RADIATION AND POLARIZATION SIGNATURES OF THE 3D MULTIZONE TIME-DEPENDENT HADRONIC BLAZAR MODEL

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ABSTRACT

We present a newly developed time-dependent three-dimensional multizone hadronic blazar emission model. By coupling a Fokker–Planck-based lepto-hadronic particle evolution code, 3DHad, with a polarization-dependent radiation transfer code, 3DPol, we are able to study the time-dependent radiation and polarization signatures of a hadronic blazar model for the first time. Our current code is limited to parameter regimes in which the hadronic γ-ray output is dominated by proton synchrotron emission, neglecting pion production. Our results demonstrate that the time-dependent flux and polarization signatures are generally dominated by the relation between the synchrotron cooling and the light-crossing timescale, which is largely independent of the exact model parameters. We find that unlike the low-energy polarization signatures, which can vary rapidly in time, the high-energy polarization signatures appear stable. As a result, future high-energy polarimeters may be able to distinguish such signatures from the lower and more rapidly variable polarization signatures expected in leptonic models.

Key words: galaxies: active – galaxies: jets – gamma rays: galaxies – polarization – radiation mechanisms: nonthermal – relativistic processes

1. INTRODUCTION

Blazars are the most violent class of active galactic nuclei. Their emission is known to be nonthermal-dominated, covering the entire electromagnetic spectrum from radio up to TeV γ-rays, with strong variability on all timescales (e.g., Aharonian et al. 2007). Blazar spectral energy distributions (SEDs) are characterized by two broad, nonthermal components. The low-energy component, from radio to optical−UV, is generally agreed to be synchrotron radiation of ultrarelativistic electrons. The origin of the high-energy component, from X-rays to γ-rays, is still under debate. The leptonic model argues that the high-energy component is due to the inverse Compton scattering of either the low-energy synchrotron emission (SSC; e.g., Marscher & Gear 1985; Maraschi et al. 1992) or external photon fields (EC; e.g., Dermer et al. 1992; Sikora et al. 1994), while the hadronic model suggests that the high-energy emission is dominated by synchrotron emission of ultrarelativistic protons and the cascading secondary particles resulting from photo-pion and photo-pair-production processes (e.g., Mannheim & Biermann 1992; Mücke & Protheroe 2001). It is of high importance to many aspects of high-energy astrophysics to distinguish these two models, because it will put strong constraints on the blazar jet power, the physics of the central black hole, and the origin of ultra-high-energy (UHE) cosmic rays and very high energy (VHE, i.e., TeV−PeV) neutrinos. However, both models are generally able to produce reasonable fits to snapshot SEDs of blazars (e.g., Böttcher et al. 2013). Thus, additional diagnostics are necessary.

An obvious choice would be through the identification of blazars as the sources of VHE neutrinos, which are the “smoking gun” of hadronic interactions (e.g., Halzen & Zas 1997; Kistler et al. 2014; Diltz et al. 2015; Petropoulou et al. 2015). IceCube has reported detection of astrophysical VHE neutrinos, and there are hints that the origin of these neutrinos could be spatially connected to blazars (e.g., Aartsen et al. 2013; Kadler et al. 2016). However, in view of the low angular resolution of IceCube, so far the sources of these neutrinos are still unknown.

An alternative is the study of light curves. The development of time-dependent leptonic models has been quite fruitful (e.g., Joshi & Böttcher 2011; Diltz & Böttcher 2014; Asano & Hayashida 2015; Weidinger & Spanier 2015). Although one-zone leptonic models sometimes have difficulty in explaining the frequently seen symmetric light curves, some multizone leptonic models that explicitly include the light-travel-time effects (LTTEs) have successfully resolved that issue (e.g., Chen et al. 2014). On the other hand, due to the more complicated cascading processes, hadronic models are generally stationary and/or single-zone (e.g., Mastichiadis & Kirk 1995; Cerruti et al. 2015; Yan & Zhang 2015).

Another possible discriminant is that leptonic and hadronic models require very distinct magnetic field conditions. Radio to optical polarization measurements have been a standard probe of the jet magnetic field. In particular, recent observations of γ-ray flares with optical polarization angle (PA) swings and substantial polarization degree (PD) variations indicate the active role of the magnetic field during flares (e.g., Marscher et al. 2008; Abdo et al. 2010; Blinov et al. 2015). Several models have been put forward to explain these phenomena (e.g., Larionov et al. 2013; Marscher 2014; Zhang et al. 2015), and a first-principle magnetohydrodynamics (MHD) based model is also under development (Zhang et al. 2016). For the high-energy emission, Zhang & Böttcher (2013) have shown that by combining the infrared/optical and the X-ray/γ-ray polarization signatures, it would be possible to distinguish the two models. Several X-ray and γ-ray polarimeters are currently proposed and/or under development (e.g., Hunter et al. 2014). However, despite remarkable progress that has been made to improve these high-energy polarimeters, they commonly suffer from limited sensitivity. If the high-energy
polarization signatures vary as rapidly as the low-energy (optical) polarization, it will be difficult for these polarimeters to measure, as they will integrate over episodes of vastly different PAs. This prompted us to investigate the time-dependent high-energy polarization signatures of leptohadronic blazar models in more detail.

In this paper, we present a newly developed 3D multizone time-dependent hadronic model code, 3DHad. This new code is based on the one-zone time-dependent Fokker–Planck (FP) based leptohadronic code of Diltz et al. (2015), but generalized to 3D multizone. By coupling with the 3D polarization-dependent ray-tracing routines of the 3DPol code developed by Zhang et al. (2014), we will derive the time-dependent radiation and polarization signatures across the whole blazar SED, including all LTTEs. Hence, we can study the general phenomenology of the light curves and time-dependent polarization signatures. Hadronic models generally require very high jet powers and magnetic fields. Therefore, we will put physical constraints on the allowed parameter space by estimating the available jet power and magnetic field in the case of a Blandford–Znajek (Blandford & Znajek 1977) powered jet. With the above consideration, we will predict detailed time-dependent polarization signatures from proton-synchrotron-dominated hadronic models based on various jet conditions and flaring mechanisms. These results can be compared with multiband radiation and future high-energy polarization measurements, putting stringent constraints on the blazar jet conditions in a hadronic model. We will describe our code setup and physical considerations in Section 2, sketch our model setup in Section 3, present case studies in Sections 4 and 5, and discuss the results in Section 6.

2. 3DHad AND PHYSICAL CONSIDERATIONS

In this section, we will first introduce 3DHad and its main features and how it is coupled with 3DPol. Then we will justify the physical considerations for the hadronic model and put constraints on the parameter space. Finally, for code verification purposes, we will compare 3DHad with the one-zone hadronic code developed by Diltz et al. (2015) and illustrate the similarities and differences.

2.1. Code Features

3DHad is a time-dependent multizone nonthermal electron and proton evolution code based on FP equations. The code is written in a module-oriented style in FORTRAN 95, fully parallelized by MPI. This code can directly take inputs of each zone, including geometry, magnetic field information, particle evolution, etc., either from inhomogeneous blazar model parameters or from first-principle simulations such as MHD and particle-in-cell (PIC) simulations. Based on the inputs, each zone will solve FP equations for the evolution of electron and proton energy distributions. In this first application that we present here, we will not consider any particle transfer between the zones; hence, the FP equations in each zone are independent.

We apply an implicit Euler method to solve the FP equations numerically. The solutions of FP equations in each zone are based on the work by Diltz et al. (2015). The general form of the FP equation is

$$\frac{\partial n(\gamma, t)}{\partial t} = \frac{\partial}{\partial \gamma} \left( K_{\gamma} \frac{\partial n(\gamma, t)}{\partial \gamma} \right) - \frac{\partial}{\partial \gamma} \left( (\gamma + 2K_{\gamma}) n(\gamma, t) \right) - \frac{n(\gamma, t)}{t_{\text{esc}}} + n_{\text{inj}}(\gamma, t),$$

where $K = 1/(2t_{\text{acc}})$. The underlying assumption in Equation (1) is that the particle evolution is governed by four processes: a fast first-order Fermi acceleration process characterized by $n_{\text{inj}}(\gamma, t)$, a second-order Fermi acceleration process characterized by a mass-independent acceleration timescale $t_{\text{acc}}$, the synchrotron cooling on $\gamma$, and particle escape parameterized by an energy-independent escape timescale $t_{\text{esc}}$. In a steady, quiet state, nonthermal particles are continuously injected into each zone with a power-law distribution in energy,

$$n_{\text{inj}}(\gamma, t) = n_0 \times \gamma^{-\alpha}, \quad \gamma_{\text{min}} < \gamma < \gamma_{\text{max}},$$

which represents a rapid particle acceleration mechanism, such as diffusive shock acceleration and magnetic reconnection (Guo et al. 2016) on timescales much shorter than the time resolution of our simulation. In addition to this process, the emission region may contain microscopic turbulence, which will mediate stochastic second-order Fermi acceleration. We take $t_{\text{acc}} = 1/\alpha$ as the stochastic acceleration timescale, where $\alpha = (d\gamma/dt)/\gamma$ is the stochastic acceleration rate. The exact form of $\alpha$ depends on the turbulent acceleration model and the turbulence parameters. A detailed treatment of these aspects is beyond the scope of this paper. Here we simply take $t_{\text{acc}}$ to be independent of particle energy. In general, the Compton cooling rates in hadronic models are negligible compared to synchrotron losses due to the large magnetic fields (e.g., Böttcher et al., 2013), especially in the parameter space that we will employ here. Finally, since we do not consider particle transport between zones in this first application, we simply use an energy-independent escape timescale $t_{\text{esc}}$ to mimic the process in which particles leave a particular zone and no longer contribute to the emission there.

While the original one-zone hadronic code in Diltz et al. (2015) is very comprehensive, including all details of pion production, $\gamma-\gamma$ interactions, explicit muon and pion evolution, etc., in this paper we will restrict the parameters to a regime in which the proton energy losses andradiative outputs are strongly dominated by proton synchrotron emission, thus neglecting photo-pion and photo-pair-production processes, and following only the electron and proton evolution. In this way, the photon transfer between each zone will not affect the particle evolution. The parameter restrictions inherent in this assumption will be detailed in the next section.

3DHad solves the FP equations for the particle distributions in each zone at each time step; in order to calculate the resulting emission, the derived time-dependent particle distributions will be fed into 3DPol (Zhang et al. 2014), which has been upgraded to include synchrotron emission (and their polarization signatures) from heavier particles, such as protons. 3DPol can calculate the time-dependent radiation and polarization signatures based on the particle and magnetic field inputs. Since in the parameter regime adopted here Compton scattering
is negligible, radiation transfer between zones will not affect the particle evolution. Hence, the radiation transfer problem is reduced to a ray-tracing method. The gyroradius of a proton is given by

$$r_g = \frac{\gamma_p m_p c^2}{eB} \sim 3 \times 10^6 \frac{\gamma_p}{B(G)} \text{ cm.}$$  \hspace{1cm} (3)

For a magnetic field of $B \sim 10$ G and the most energetic protons around $\gamma \sim 10^5$, this yields a gyroradius of the order of $\sim 10^{14}$ cm, which is smaller than our spatial resolution in the emission region. Therefore, we can assume that all particles will radiate in their corresponding zones and calculate the individual Stokes parameters in each zone. By adding up the ones that arrive at the observer at the same time, we naturally include all LTTEs.

The execution of the combined 3DHad and 3DPol is efficient. For the runs that we will show in this paper, they take about 20 minutes on 500 CPUs on LANL clusters. Therefore, the code has the potential to do larger runs for more detailed physical modeling, e.g., with physical conditions derived from MHD simulations.

2.2. Physical Constraints and Assumptions

Hadronic blazar models usually require high magnetic fields and nonthermal particle energies close to the upper limits that blazars can plausibly provide based on our current understanding of accretion and jet formation processes (e.g., Böttcher et al. 2013; Cerruti et al. 2015; Zdziarski & Böttcher 2015). Here we estimate the resulting limits and put constraints on the hadronic model parameter space. We employ the conservation of magnetic flux in the jet to estimate the available magnetic field in the emission region, and the Eddington luminosity to constrain the total particle energy. The magnetic flux from the Blandford–Zhakaj mechanism is given by

$$\Phi_B \sim 1.4 \times 10^{33} \frac{1}{f_0(a)} L_{46} M_9 \text{ G cm}^2,$$  \hspace{1cm} (4)

where $f_0(a) = a/(1 + \sqrt{1 - a^2})$ and $a$ is the dimensionless spin parameter of the black hole, $L_{46}$ is the magnetic jet luminosity in units of $10^{46}$ erg s$^{-1}$, and $M_9$ is the black hole mass in units of $10^9$ M$_\odot$. Assuming conservation of the poloidal magnetic flux along the jet, and that the poloidal component is comparable to the toroidal component, the magnetic flux in the emission region is approximated by $B \pi R^2$, where $R = 10^{16} R_6$ cm is the radius of the emission region. Given a bright blazar ($L_{46} \sim 100$) and a large central black hole mass ($M_9 \sim 1$), we find the first constraint,

$$B \times R^2 \lesssim 10^{33} \text{ G cm}^2$$  \hspace{1cm} (5)

or $B \lesssim 10 R_6^{-2} G$. Assuming bulk motion of the blazar emission region with a Lorentz factor $\Gamma \gg 1$, the kinetic luminosity in protons is evaluated by

$$L_p \sim \pi R^2 \Gamma^2 c u_p,$$  \hspace{1cm} (6)

where $u_p = m_p c^2 \int_0^\infty d\gamma n_p(\gamma) \gamma$ is the proton energy density in the rest frame of the emission region, and $n_p(\gamma)$ is the proton spectral number density in that frame. We expect that the total proton kinetic luminosity should not exceed the Eddington luminosity, which is given by

$$L_{\text{Edd}} = 4\pi G M_p c / \sigma_T \sim 1.2 \times 10^{47} M_9 \text{ erg s}^{-1}.$$  \hspace{1cm} (7)

With a bulk Lorentz factor $\Gamma$ of a few tens, and using the same black hole mass as in Equation (5), we obtain the second constraint,

$$u_p \times R^2 \lesssim 10^{33} \text{ erg cm}^{-1}.$$  \hspace{1cm} (8)

In spite of significant uncertainties in constraints on physical conditions in blazars, Equations (5) and (8) allow us to put some stringent constraints on parameters to be used for our models. For instance, hadronic models typically require magnetic fields exceeding 10 G (e.g., Böttcher et al. 2013; Cerruti et al. 2015). Hence, by Equation (5), the size of the emission region in the comoving frame should generally be smaller than $10^{16}$ cm, which can be translated to a flare duration of $\sim 10$ h in the observer’s frame, assuming a typical Lorentz factor of $\Gamma \sim 20$. Therefore, flares that last several days, in particular in the low-energy bands such as optical, where the LTTEs generally dominate, are unlikely to be of hadronic origin, unless some general physical conditions are varying on longer timescales. We will demonstrate this point in Sections 4 and 5.

For this preliminary study, we will make some additional assumptions in order to avoid more complicated radiation-feedback calculations, so that only the electron and proton evolution is important. The assumptions are as follows:

1. Proton and electron energy losses are dominated by synchrotron cooling;
2. $\gamma \gamma$ opacity and pair production are negligible.

This restricts the parameter space in which our model is applicable, as detailed in the following.

For assumption 1, we need to make sure that the synchrotron cooling for protons should be faster than the pion-production cooling rate. The synchrotron loss rate for protons is given by

$$\dot{\gamma}_{p,\text{syn}} = \frac{6\pi\sigma_T B^2}{m_e c^6} \left( \frac{m_e}{m_p} \right)^3 \gamma_p^2$$  \hspace{1cm} (9)

and the pion production loss rate is given by (Aharonian 2000)

$$\dot{\gamma}_{p,\pi} = -\epsilon (\langle \sigma_{\gamma \pi} f \rangle) n_{\text{ph}}(\epsilon)^* \epsilon^* \gamma_p$$  \hspace{1cm} (10)

where $\langle \sigma_{\gamma \pi} f \rangle \sim 10^{-28} \text{ cm}^2$ represents the elasticity-weighted $p\gamma$ interaction cross section, $\epsilon^* = 5.9 \times 10^{-8} E_{19}^{-1}$ represents the energy of target photons interacting with protons of energy $E = 10^{19} E_{19} \text{ eV}$ at the $\Delta$ resonance, and $n_{\text{ph}}(\epsilon)$ represents the target photon field for photo-pion production in units of photon energy normalized with respect to the rest mass of the electron, $\epsilon = \hbar \nu / m_e c^2$. For a typical set of parameters of a hadronic blazar model, the two energy loss rates are plotted in Figure 1. By comparing the two rates, we find that synchrotron losses dominate for protons with Lorentz factors

$$\gamma_p > \frac{6\pi m_e c^2 \langle \sigma_{\gamma \pi} f \rangle n_{\text{ph}}(\epsilon)^* \epsilon^*}{\sigma_T B^2} \left( \frac{m_p}{m_e} \right)^3.$$  \hspace{1cm} (11)

Assuming that the relevant section of the target synchrotron photon spectrum in the comoving frame is in the form of a power law, $n_{\text{ph}}(\epsilon) = n_{\text{ph}}^0 \epsilon^{-\alpha}$, the above constraint can be
Figure 1. Synchrotron and pion-production loss rates of a power-law proton distribution with cutoffs $\gamma_{\text{min}} = 1.0$, $\gamma_{\text{max}} = 10^5$, spectral index $p_\gamma = 2.2$ in an emission region of size $R = 10^6 \text{cm}$, and magnetic field of $B = 50 \text{G}$. Synchrotron losses generally dominate over pion-production losses for ultrarelativistic protons.

written as

$$\gamma_p > \frac{6\pi m_e c^2 \langle \sigma_T \gamma \rangle n_{\text{ph}}^0 (\epsilon^*)^{1-\alpha} (m_p/m_e)^3}{\sigma_T B^2},$$  \hfill (12)$$

For the highest-energy protons typically used in the leptohadronic modeling of flat-spectrum radio quasars (FSRQs), $\gamma_{p,\text{max}} \approx 10^8$, the most efficient target photons for pion production have energies of $\epsilon^* = 590/\gamma_p \sim 6.0 \times 10^{-6}$. This is generally in the optical and UV bands, which are dominated by electron synchrotron emission. Using the delta approximation for the synchrotron power of electrons (Böttcher et al. 2012) and assuming a steady-state electron distribution in the form of a power law, the constraint can then be rewritten in terms of the model parameters,

$$\left(10^{-17} B(G) \gamma_p\right)^{\nu_e} n_{0,e}(\text{cm}^{-3}) R{(\text{cm})} < 10^{22},$$  \hfill (13)$$

where $n_{0,e}$ is the normalization factor of the electron distribution, $p_e$ is the electron power-law index, $R$ is the radius of the emission region, and $\gamma_p$ is the proton Lorentz factor. As we can see, for a soft electron spectrum, $\nu_e \geq 3$, given the physical constraints of Equations (5) and (8), the above equation generally holds for all proton energies that significantly contribute to the radiative output. For a hard electron spectrum, $\nu_e \lesssim 3$, the low-energy protons may be subject to dominant pion-production losses. However, the total radiative output of these low-energy protons will be negligible compared to the output by ultrarelativistic protons ($\gamma_p \gtrsim 10^7$) and can therefore be safely neglected.

Assumption 2 requires that the $\gamma \gamma$ optical depth satisfies $\tau_{\gamma \gamma}(\epsilon_1) < 1$. This implies a minimum Doppler factor of

$$\delta_D > \sqrt{\frac{\tau_{\gamma \gamma}}{\sigma_T}} \int f_{p_k}^{\text{pk}} (1+z)^2 \epsilon_1^{\text{obs}} \frac{4m_e c^2 t_v}{4m_e c^2 t_v},$$  \hfill (14)$$

(Dondi & Ghisellini 1995), where $d_L$ represents the luminosity distance of the source, $\epsilon_1^{\text{obs}}$ represents the highest observed energy of $\gamma$-ray photons, $f_{p_k}^{\text{pk}}$ represents the observed flux of target photons, and $t_v$ represents the variability timescale. The energy of the observed target photons in terms of the observed $\gamma$-ray photon energy is given by $\epsilon_1^{\text{obs}} = 2\delta_D^2/[(1+z)^2 \epsilon_1^{\text{obs}}]$. The observed flux at energy $\epsilon$ can be written in terms of the synchrotron photon field in the comoving frame of the jet,

$$f_\epsilon = \epsilon F_\epsilon = \frac{\delta_D^2 m_e c^2 V_b \epsilon^2 n_{\text{ph}}(\epsilon)}{4\pi d_L^2 t_v},$$  \hfill (15)$$

where $t_v$ is the light-crossing timescale and $V_b$ represents the comoving volume of the emission region. High-energy $\gamma$-rays of blazars typically peak around $\epsilon_1^{\text{obs}} \sim 1000$. The characteristic energy of target photons for pair production in an FSRQ, such as 3C 279, is then $\epsilon_1^{\text{obs}} = 2\delta_D^2/[(1+z)^2 \epsilon_1^{\text{obs}}] \sim 0.33$, which is in the hard X-ray band. This suggests that proton synchrotron emission represents the primary target photon field for pair production. Assuming that the target photon field is in the form of a power law, the constraint of Equation (14) can be rewritten as

$$\delta_D > \frac{1}{6} \sigma_T n_{\text{ph}}^0 R e^{1-\alpha}(1+z).$$  \hfill (16)$$

Again we apply the delta approximation for the synchrotron power of protons (Böttcher et al. 2012), and assuming a steady-state proton distribution in the form of a power law, the constraint can then be rewritten in terms of the hadronic model parameters

$$\delta_D \gtrsim 10^{-51}(10^{-17}) p_e^{-2} R^2 B n_{0,p} \gamma_\text{max},$$  \hfill (17)$$

where $R$ is in units of cm, $B$ in units of G, and $n_{0,p}$ in units of cm$^{-3}$. With the physical constraint in Equation (8) and a typical Doppler factor of $\sim 20$, the above constraint is satisfied for all parameter combinations employed in this study.

Additionally, as has been shown in many hadronic fittings (e.g., Böttcher et al. 2013; Cerruti et al. 2015), Compton scattering generally does not make a substantial contribution due to the large magnetic field; hence, we will also neglect this effect here.

2.3. Comparison with One-zone Code

In order to verify the validity of our multizone hadronic radiation transfer approach, we compare the results of the one-zone code of Diltz et al. (2015) with the results obtained with 3DHad+3DPol. We consider two sets of parameters for the quiescent state, sets 1 and 2, as listed in Table 1. These parameters refer to the pre-flare equilibrium state, where all cells are characterized by the same set of parameters. The difference between these two parameter sets is that set 1 has particle evolution timescales generally larger than the light-crossing timescale, while in set 2 the light-crossing timescale is generally the longest relevant timescale. Both parameter sets obey the constraints derived above. In order to examine the flare features, we change the proton injection density rate for the entire emission region after equilibrium has been achieved: for set 1, we choose $\dot{u}_{p,\text{inj}} = 1.2 \times 10^{-2} \text{erg s}^{-1} \text{cm}^{-3}$; for set 2, $\dot{u}_{p,\text{inj}} = 1.5 \times 10^{-5} \text{erg s}^{-1} \text{cm}^{-3}$.
The purpose of this paper is to study the general radiation and polarization signatures of hadronic blazar models. To show the most generic features of such models, we employ a simple model setup with the least physical assumptions. We assume that a cylindrical emission region travels relativistically in a straight trajectory along the jet, when it encounters a flat stationary disturbance, resulting in a flare. While we are observing blazars at a small observing angle $\theta_{\text{obs}}$ along the jet in the observer’s frame, due to relativistic aberration, the observing angle $\theta_{\text{obs}}^\ast$ is much larger in the comoving frame of the emission region. Specifically, if $\theta_{\text{obs}}^\ast = 1/\Gamma$, where $\Gamma$ is the Lorentz factor of the emission region in the observer’s frame, then $\theta_{\text{obs}} = 90^\circ$ for $\Gamma \gg 1$. As observations frequently suggest $\theta_{\text{obs}}^\ast \sim 1/\Gamma$, we will choose $\theta_{\text{obs}} = 90^\circ$. In this case, the Doppler factor is $\delta \equiv (\Gamma^2 [1 - \beta^2 \sin^2 \theta_{\text{obs}}^\ast]^{-1} = \Gamma$.

In the comoving frame, the emission region is pervaded by a helical magnetic field. For this preliminary study, we will not add any turbulent field component. While a turbulent magnetic field is likely to dominate the polarization fluctuations occurring mostly in the quiescent state (Marscher 2014), during major flares the polarization signatures appear more systematic, indicating a deterministic process (e.g., Abdo et al. 2010; Blinov et al. 2015; Kiehlmann et al. 2016). Zhang et al. (2015) have explicitly demonstrated that in such cases, the addition of a turbulent field component indeed yields a better fit to the observational data, but the general trends of radiation and polarization signatures are similar to a purely helical field.

The disturbance will propagate through the emission region in the comoving frame. The zones affected by the disturbance will have different physical conditions from the initial state. After the disturbance moves out of a given zone, the zone will revert to its initial conditions. We point out that while the physical conditions such as the stochastic acceleration and the nonthermal particle injection can reasonably return to the quiescent state after the passage of the disturbance, this is not necessarily the case for the magnetic field strength and topology. However, the polarization signatures are frequently observed to quickly return to the initial values even after major variations such as PA swings (e.g., Abdo et al. 2010; Morozova et al. 2014; Blinov et al. 2015, 2016), indicating the restoration of the magnetic field. Zhang et al. (2016) have shown that this restoration is only possible when there is substantial magnetic energy compared to the plasma kinetic energy in the emission region. In most hadronic models, the magnetic energy is comparable to or stronger than the kinetic energy (e.g., Böttcher et al. 2013). In particular, the parameter sets we will use in the following satisfy this condition.

Due to the LTTEs and the chosen $\theta_{\text{obs}}^\ast$, although the disturbance is flat, the observed “flaring region” will appear different. Figure 3 shows a sketch of our model, especially the shapes of the flaring regions when the disturbance propagates through various locations in the emission region. The flaring region is composed of an “active region,” with a slanted, ellipsoidal shape due to LTTEs, and an “evolving region,” which is due to the slow evolution of protons. The zones outside the flaring region are termed as the “quiescent region.” The impact of the LTTEs on the polarization signatures has been discussed in detail in Zhang et al. (2014, 2015).

### Table 1

| Parameters | Set 1 | Set 2 |
|------------|------|------|
| Bulk Lorentz factor $\Gamma$ | 20.0 | 20.0 |
| Orientation of LOS $\theta_{\text{obs}}$ (°) | 90 | 90 |
| Radius of the emission region $R$ (10^6 cm) | 1.0 | 9.0 |
| Height of the emission region $Z$ (10^6 cm) | 1.33 | 12.0 |
| Acceleration timescale $t_{\text{acc}}$ (10^6 s) | 8.2 | 2.9 |
| Escaping timescale $t_{\text{esc}}$ (10^6 s) | 2.0 | 1.5 |
| Background injection electron density rate $\dot{\nu}_{\text{e,inj}}$ (erg s^{-1} cm^{-3}) | $2.8 \times 10^{-7}$ | $3.9 \times 10^{-10}$ |
| Background injection electron minimum energy $\gamma_{\text{e, min}}$ | 100 | 80 |
| Background injection electron maximum energy $\gamma_{\text{e, max}}$ | 10000 | 3500 |
| Background injection proton density rate $\dot{\nu}_{\text{p,inj}}$ (erg s^{-1} cm^{-3}) | $3 \times 10^{-3}$ | $1.9 \times 10^{-6}$ |
| Background injection proton minimum energy $\gamma_{\text{p, min}}$ | 1 | 1 |
| Background injection proton maximum energy $\gamma_{\text{p, max}}$ | $5 \times 10^{8}$ | $3 \times 10^{8}$ |
| Background injection proton spectral index $p_p$ | 2.2 | 2.2 |
| Helical magnetic field $B$ (G) | 50.0 | 80.0 |
| Magnetic pitch angle $\theta_\phi$ (deg) | 45 | 45 |

**Note.** Except for the Lorentz factor, which is in the observer’s frame, all parameters are in the comoving frame of the emission region. The time resolution is always identical to the typical light-crossing time of a zone. Due to the small size of the emission region in parameter set 1, it is computationally expensive to obtain high time resolution. The resulting light curves and polarization signatures, however, due to the implicit Euler method employed to solve the Fokker–Planck equations, we still obtain stable solutions for relatively large time steps (see Figures 4–10).
The parameter sets 1 and 2 described in the previous section characterize the quiescent states for the following studies. We choose the same size of the disturbance in all the following case studies, which is 0.25 times the length of the cylindrical emission region, so that the disturbance propagation timescale in a specific zone is $t_{\text{prop}} = 0.25t_{\text{lc}}$. We consider four scenarios in the active region that give rise to flares due to the disturbance:

a. Magnetic energy dissipation, where the magnetic field strength will decrease and its topology will change, along with additional particle injection;
b. Magnetic compression, where the magnetic field strength will increase and change its topology;
c. Enhanced particle injection for both electrons and protons;
d. Enhanced stochastic acceleration, where the stochastic acceleration timescale becomes shorter.

The flaring parameters for these scenarios are listed in Table 2. The parameter sets 1 and 2 described in the previous section characterize the quiescent states for the following studies. We choose the same size of the disturbance in all the following case studies, which is 0.25 times the length of the cylindrical emission region, so that the disturbance propagation timescale in a specific zone is $t_{\text{prop}} = 0.25t_{\text{lc}}$. We consider four scenarios in the active region that give rise to flares due to the disturbance:

4. SYNCHROTRON COOLING AND LTTEs

In this section, we will study scenario a, magnetic energy dissipation to illustrate the effect of the relation between synchrotron cooling timescales and LTTEs (Figures 4 and 5). Guo et al. (2016) have performed comprehensive PIC simulations to show that both electrons and protons can be effectively accelerated during magnetic reconnection events. As the detailed simulation of a reconnection event is beyond the scope of this paper, we simply assume that the particle injection is enhanced and the magnetic field is weakened in the disturbance, and we keep the particle injection index the same as in the quiescent state. We have not included any thermal radiation contributions to the multiwavelength emission, such as the big blue bump typically seen in the FSRQs, or the host galaxy. In this way, the difference in the time-dependent radiation and polarization signatures mostly originates from the intrinsic hadronic physics. Proton synchrotron cooling is much slower than that for electrons. Due to the strong magnetic field, the electron cooling timescale ($t_{\text{ec}}$) is generally shorter than the light-crossing timescale ($t_{\text{lc}}$). Moreover, as is shown in Equation (5), the size of the emission region in the hadronic...
model has an upper limit due to the magnetic-flux constraint. Thus, in most applicable situations, the proton cooling timescale \( t_{pc} \) is comparable to or longer than \( t_{lc} \). In the following, we will demonstrate that this timescale relation, \( t_{ec} \approx t_{lc} < t_{pc} \), which is largely intrinsic to the hadronic model without any strong parameter dependence, is governing the general shape of the light curves and polarization signatures.

4.1. Case 1a

This case refers to a small emission region (baseline parameter set 1) with magnetic energy dissipation (flaring scenario a) and is illustrated in Figure 4. Since we do not vary the power-law index for the enhanced particle injection, the SEDs (Figure 4, upper left) generally keep the same spectral indices during flares. In the quiescent state, the PD versus photon energy (Figure 4, upper right) displays minor fluctuations across the entire spectrum. However, during the flare, we notice considerable spectral PD variations. These are shown in more detail in the time evolution of radiation and polarization signatures (middle and bottom panels of Figure 4).

Before we move to the emission evolution, we first take a look at the particle evolution. Figure 6 presents the electron (upper left) and proton (upper right) spectral evolution for Case 1a. In the electron evolution, owing to the short \( t_{ec} \), after the disturbance leaves a certain zone, most electrons only take about a disturbance propagation timescale \( t_{dp} \) to revert to the pre-flare equilibrium. However, the lowest-energy electrons have longer synchrotron cooling timescales; thus, they take longer (up to \( \sim 4t_{dp} = 1t_{lc} \)) to revert to the quiescent state. Therefore, the evolving region for the electrons is comparable to the active region, except for the lowest-energy electrons, where it is moderately larger. The proton evolution appears very different. In view of the much longer cooling timescale \( t_{pc} \), after about 20\( t_{dp} \), the proton synchrotron contribution from the evolving region no longer dominates the active region, and it takes about 60\( t_{dp} \) (i.e., about 15\( t_{lc} \)) to evolve back to a state.

**Figure 3.** Sketch of the model and LTTEs. Left: a disturbance propagates through the emission region pervaded by a helical magnetic field in its comoving frame. Red, green, and blue colors denote the location of the disturbance at approximately entering the emission region \( t_1 \), leaving the emission region \( t_2 \), and some time after leaving the emission region \( t_3 \), respectively. Right: the corresponding flaring region at \( t_1 \) to \( t_3 \) at equal photon-arrival times at the observer. Dashed shaded regions are the active region; the region between the dashed shaded region and the dotted shape is the evolving region.

**Table 2**

| Parameters | Case 1a | Case 2a | Case 1b | Case 1c | Case 2c | Case 1d |
|------------|---------|---------|---------|---------|---------|---------|
| \( t_{acc,d} (10^8 \text{ s}) \) | ... | ... | ... | ... | ... | 0.51 |
| \( n_{e,inj,d} (\text{erg s}^{-1} \text{cm}^{-3}) \) | \( 3.0 \times 10^{-6} \) | \( 4.1 \times 10^{-9} \) | ... | \( 1.6 \times 10^{-6} \) | \( 2.2 \times 10^{-9} \) | ... |
| \( n_{p,inj,d} (\text{erg s}^{-1} \text{cm}^{-3}) \) | \( 5.5 \times 10^{-2} \) | \( 9.8 \times 10^{-6} \) | ... | \( 5.5 \times 10^{-2} \) | \( 9.6 \times 10^{-6} \) | ... |
| \( B_d (G) \) | 36.6 | 58.6 | 136.6 | ... | ... | ... |
| \( \theta_{bd} (\text{deg}) \) | 75 | 75 | 75 | ... | ... | ... |

**Note.** Only the parameters that are varied in the case studies are listed here. All parameters have the same meaning as in Table 1, except for the subscript \( d \), which denotes the parameters at the disturbance.
close to the quiescent equilibrium. Hence, for protons the evolving region overwhelms the active region. These features are clearly reflected in light curves and polarization variations. For the low-energy component, since the evolving region for electrons is relatively small, the LTTEs will be dominating. Thus, the flaring region on the right side of the sketch in Figure 3 is generally similar to that on the left side. Therefore, the light curves from radio to UV appear generally symmetric in time (Figure 4, middle left). However, due to the slightly longer $t_{\text{ee}}$ for the lowest-energy electrons, which are responsible for the radio emission, the radio peaks a little bit later than the optical and UV. Unlike the light curves, which only depend on the luminosity, the polarization signatures are also affected by the PD and PA in each zone. As the magnetic field structure varies from the active region to the evolving and the quiescent region, even in the PD and PA of the optical and UV bands we find a small degree of asymmetry in time. We notice that both the optical and UV bands exhibit a PA swing and significant PD variations (Figure 4, middle and lower right). This is consistent with the
results of Zhang et al. (2014, 2015), where these effects are discussed in detail.

The evolving region for protons region dominates the high-energy emission. All light curves peak considerably later than the low-energy light curves; in particular, we find long cooling tails in the high-energy light curves, which strongly extend the flare duration (Figure 4, lower left). In the polarization signatures, we only find small changes in both PD and PA (Figure 4, middle and lower right), due to the strong contamination from the evolving region, which has the same magnetic topology as the quiescent region. Specifically, at the beginning of the flare, as the evolving region is very small, the PD shows a relatively large drop. After that, the evolving region becomes dominant; hence, the polarization gradually recovers its initial state. When the active region has completely moved out, approximately at the same time when the low-energy flare stops, the high-energy polarization signatures appear largely identical to the quiescent state.

4.2. Case 2a

The major difference of case 2a (baseline parameter set 2) compared to case 1a lies in the longer light-crossing time, $t_{lc}$. Again, we examine the particle evolution (Figure 6, lower panel). When the disturbance moves out of a certain zone, most electrons revert to the quiescent equilibrium immediately, except for the electrons responsible for the radio emission, which take up to about $0.5t_{dp}$ to recover. Thus, the evolving region is generally smaller than the active region. For protons, after the disturbance leaves, they continue to make a substantial contribution to the high-energy emission for $\sim 3t_{dp} = 0.75t_{dp}$.
although it takes $\sim 7T_{\text{dp}}$ to fully recover to equilibrium. Hence, the evolving region is moderately larger than the active region.

Consequently, in the low-energy component, all light curves and polarization signatures appear symmetric in time without any noticeable delay (Figure 5, middle left); additionally, all bands display PA swings, although the radio polarization slightly diverges from the others (Figure 5, middle and lower right). In the high-energy component, the light curves appear generally symmetric in time, though they still peak later and the flares last longer than in the low-energy light curves (Figure 5, lower left). Nevertheless, the polarization contamination from the evolving region is still significant; thus, there is no PA swing in the high-energy bands (Figure 5, middle and lower right). We notice that unlike the light curves, the high-energy polarization signatures are still synchronized with the low-energy flares and polarization variations: they all end approximately when the active region moves out.

To summarize this section, we find that the combined effects of synchrotron cooling and LTTEs will result in some interesting features in the hadronic models. First, the polarization signatures in the high-energy component are nearly identical from X-rays to $\gamma$-rays. Therefore, X-ray and $\gamma$-ray polarimeters may both be able to measure hadronic signatures in the high-energy polarization. Additionally, in the quiescent state, if the electrons and protons reside in the same emission region, the high-energy polarization signatures should be generally identical to the low-energy component. Moreover, the low-energy light curves and polarization variations are generally symmetric in time, but the high-energy signatures are generally asymmetric. Also, the high-energy flares generally peak later and last longer than the low-energy flares. The low-energy flares and polarization variations, as well as the high-energy polarization variations, are generally synchronized. Finally, while the low-energy polarization signatures may vary rapidly during flares, high-energy polarization signatures appear generally stable.

5. CASE STUDY OF ALTERNATIVE FLARING SCENARIOS

In this section, we present more case studies to further test the hadronic features listed in the previous section, and we examine how the different flaring mechanisms may affect the radiation and polarization signatures. We notice that the radio emission from blazars is generally dominated by the large-scale jets instead of the local emission region; therefore, we will not show the radio signatures in the following. Moreover, the optical and UV bands appear identical; the same applies to the keV, MeV, and GeV bands. Thus, in the following we will only
take the optical and *Fermi*-LAT GeV band as representative for the low- and high-energy components, respectively, and term the GeV band simply as "\(\gamma\)-ray."

### 5.1. Scenario b

We first look at case 1b, compression of the magnetic field. In the presence of a strong magnetic field, most electrons are efficiently synchrotron cooled. This means that the electron synchrotron is already at maximal radiative efficiency. Consequently, the enhanced magnetic field will not boost the low-energy synchrotron flux, so that no flare is observed in the optical band (Figure 7, middle left). However, the active region possesses a dominant toroidal magnetic field topology, leading to a considerable drop in the PD (Figure 7, middle right).

Nevertheless, the active region does not provide additional emission; thus, the enhanced toroidal magnetic field alone is unable to trigger a PA swing (Figure 7, lower right).

On the other hand, the high-energy synchrotron component exhibits some interesting features. Due to the enhanced magnetic field in the active region, the proton cooling becomes faster, giving rise to higher flux. Additionally, after the disturbance moves out of a certain zone, the proton spectrum has a lower normalization than in the quiescent state. Hence, the evolving region actually provides less emission than the quiescent region, leading to a minor contamination in the emission signatures. This is clearly shown at the end of the flare (Figure 7, lower left), where the \(\gamma\)-ray light curve drops below the initial value. Also in the PD versus photon energy, we find...
a rapidly increasing PD tail at the highest energy, due to the exponential cooling cutoff in the proton spectrum (Figure 7, upper right). In this way, the radiation and polarization signatures during the flare are dominated by the active region. Therefore, the $\gamma$-ray light curve becomes generally symmetric in time, and there are significant and generally time-symmetric PD changes and a PA swing during the flare (Figure 7, middle and lower right).

In conclusion, the special properties in this scenario include an orphan $\gamma$-ray flare and major polarization variations in both low- and high-energy components. In particular, there may be a $\gamma$-ray PA swing. Nonetheless, we want to emphasize that in the hadronic model, the magnetic field is very strong and in most cases carries energy comparable to or even stronger than the plasma kinetic energy. In order to adequately compress the magnetic field, strong shocks are necessary, which are unlikely to happen in such a highly magnetized environment (Komissarov & Lyutikov 2011). As a result, we suggest that this scenario is unlikely in practice. For the parameter set 2, the magnetic energy is much stronger than the kinetic energy, further prohibiting this scenario. Thus, we will not discuss case 2b.

5.2. Scenario c

This is the case of enhanced particle injection at the disturbance without changing the magnetic field. Hence, the synchrotron cooling rates remain unchanged. The polarization variations in the optical band generally arise from the active region as it energizes up different parts of the emission region during its propagation (Figure 8, middle and lower right). This
has been discussed in detail in Zhang et al. (2014). On the other hand, owing to the large evolving region of the proton population, the high-energy polarization signatures again appear asymmetric in time and exhibit smaller variations than the low-energy ones. Compared to case 1a, since the magnetic field topology is unchanged, we find an increase in the PD instead (Figure 8, middle and lower right). For case 2c, LTTEs dominate. As a result, both the $\gamma$-ray light curve and the PA variability appear generally symmetric in time (Figure 9, lower). However, we can still see in the PD that the large evolving region will substantially contaminate the PD from the active region, giving rise to an asymmetric time variation (Figure 9, middle right). In conclusion, scenario c (enhanced particle injection) results in similar features to those of scenario a (particle energization by magnetic energy dissipation).

5.3. Scenario d

We finally consider scenario d, enhanced stochastic acceleration. We assume that the stochastic acceleration parameterized by $f_{\text{acc}}$, which represents the wave–particle interaction with plasma waves in the turbulence, is enhanced due to the action of a shock. In view of the very fast synchrotron cooling of electrons, even the shortened acceleration timescale is still too long to have a significant impact on the electron distribution. Hence, we observe featureless radiation and polarization signatures in the low-energy component (Figure 10, middle}

\begin{figure}[h]
\centering
\includegraphics[width=\textwidth]{figure9.png}
\caption{Case 2c. Compared to Figure 5, we removed the radio, UV, keV, and MeV bands and termed the GeV band as $\gamma$-ray. Otherwise, panels and line styles are the same as in Figure 5.}
\end{figure}
In the high-energy component, the enhanced acceleration boost the protons to higher energy, so that the SED becomes harder above a few GeV (Figure 10, upper left). However, since the total particle injection rate is kept unchanged, no major change is detected at lower energies. Otherwise, the high-energy signatures are similar to case 1c. The same applies to case 2c; hence, we will not discuss it in detail here.

We conclude that enhanced stochastic acceleration will result in a mild orphan γ-ray flare, similar to case 1b. The differences are as follows: phenomenologically, both low- and high-energy polarization signatures are stable in time, and there is no orphan flare in the X-ray band; physically, stochastic acceleration is due to magnetohydrodynamic turbulence in the emission region, whose characteristics are likely to be altered by a passing shock. Therefore, we suggest that this case is more plausible than scenario b.

6. DISCUSSIONS AND CONCLUSION

In this paper, we have presented the first 3D multizone time-dependent lepto-hadronic blazar code, 3DHad, describing a lepto-hadronic model in a parameter regime in which the high-energy emission is dominated by proton synchrotron radiation. By coupling with the 3DPol code, we are able to derive the time-dependent flux and polarization signatures of this lepto-hadronic blazar emission model, including all LTTEs. Our work thus makes the first attempt to study the time-dependent lepto-hadronic multiwavelength polarization signatures of blazar emission.
We have explicitly calculated the physical constraints for the hadronic model. Based on our estimates, if the Blandford–Znajek mechanism is responsible for powering the jet and providing the magnetic field in the jet, the hadronic emission region cannot be very large due to the limited magnetic flux that the central black hole can provide. Therefore, the largest variability timescale in the observer’s frame is unlikely to exceed a few days. Also, the high particle energy necessary for the leptohadronic scenario requires extreme jet powers. These constraints would also suggest that UHE extragalactic neutrinos are unlikely to be attributed to blazars, as photon-pion production is negligible. If the leptohadronic polarization signatures derived here are indeed detected in future observations, the required extremely efficient particle acceleration, strong magnetic field, and high jet power will seriously challenge our current understanding of AGN jet formation.

We have demonstrated that the general time-dependent signatures of our proton-synchrotron-dominated leptohadronic blazar model are dominated by the intrinsic timescale relations, namely, $f_{\text{e}} < f_{\text{b}} \lesssim f_{\text{pc}}$. Through detailed parameter studies, we have identified the following time-dependent signatures of this model:

1. The time-dependent low-energy radiation signatures are generally symmetric in time, while the high-energy signatures are generally asymmetric.
2. The high-energy flares generally peak later and last longer than the low-energy flares.
3. An orphan flare in the high-energy component is possible.
4. The polarization signatures at various wavelengths within the high-energy component are generally similar.
5. In the quiescent state, if the low- and high-energy components are co-spatial, they share similar PDs and angles.
6. While the low-energy polarization signatures may vary rapidly during flares, high-energy polarization signatures appear generally stable.
7. The time-dependent low-energy signatures and the high-energy polarization variations are generally synchronized with the disturbance propagation and the LTTEs. The high-energy flares, on the other hand, can last much longer due to the slow proton cooling.

We suggest that these features can be tested with simultaneous multiwavelength observations, including future high-energy polarimetry.

We notice that the polarization signatures possess a strong dependence on the magnetic field evolution. Although we have demonstrated in Section 3 that our assumptions on the magnetic field evolution are reasonable, our test cases are most likely an oversimplification of any actual physical scenario. However, our code can be easily coupled with first-principle simulations, such as MHD, to constrain the magnetic field evolution, so that our polarization signatures in both low- and high-energy components are physically self-consistent.

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