BLAS: Broadcast Relative Localization and Clock Synchronization for Dynamic Dense Multi-Agent Systems

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Abstract—The spatiotemporal information plays crucial roles in a multi-agent system (MAS). However, for a highly dynamic and dense MAS in unknown environments, estimating its spatiotemporal states is a difficult problem. In this paper, we present BLAS: a wireless broadcast relative localization and clock synchronization system to address these challenges. Our BLAS system exploits a broadcast architecture, under which a MAS is categorized into parent agents that broadcast wireless packets and child agents that are passive receivers, to reduce the number of required packets among agents for relative localization and clock synchronization. We first propose an asynchronous broadcasting and passively receiving (ABPR) protocol. The protocol schedules the broadcast of parent agents using a distributed time division multiple access (D-TDMA) scheme and delivers inter-agent information used for joint relative localization and clock synchronization. We then present distributed state estimation approaches in parent and child agents that utilize the broadcast inter-agent information for joint estimation of spatiotemporal states. The simulations and real-world experiments based on ultra-wideband (UWB) illustrate that our proposed BLAS cannot only enable accurate, high-frequency and real-time estimation of relative position and clock parameters but also support theoretically an unlimited number of agents.

Index Terms—Relative Localization, clock synchronization, multi-agent system, ultra-wideband, wireless sensor network.

I. INTRODUCTION

Along with the artificial intelligence tendency and the rapid development of electronic, sensor and control technologies, agents such as unmanned aerial vehicles (UAV) and unmanned ground vehicles (UGV) have been made possible to autonomously move in harsh environments and operate remotely without human intervention. Because of their flexibility, reconfigurability, and intelligence, there has been a tremendous increase in the use of such intelligent agents in tasks like target search and track [1], photovoltaic plant inspection [2], and planet exploration [3]. Over the past few years, systems containing only a single agent have been intensively investigated and used. However, the capability of a single agent is limited. In the future applications with growing complexity and uncertainty, deploying a team of small agents, namely a multi-agent system (MAS) is anticipated to offer better capabilities beyond only a single agent, in terms of robustness, scalability, and effectiveness.

Realizing this vision will require MASs to overcome some new unique challenges. Among these, real-time precise relative localization and clock synchronization are two key challenges. Relative localization is the process of determining the multi-agent dynamic topology, and clock synchronization provides a common time reference for distributed agents. The spatiotemporal determination is crucial for MASs to perform basic operations: 1) Coordination: Spatiotemporal coordination between agents is necessary for a MAS to collaboratively carry out tasks effectively. The difficulty of the coordination operations strongly lies in the knowledge of the relative position and clock parameters among the agents. If these parameters are known, effective coordination can be achieved by involving the state of all the agents at the same time [4]. 2) Data fusion: Data fusion is an essential operation to share and integrate sensory data collected by distributed agents. To fuse in a meaningful way, these data are coupled with time and location information. However, the information is expressed with respect to each agent’s local reference and needs to be transformed to a common reference. Such a transformation requires relative localization and clock synchronization of MASs. Moreover, the inter-agent collision avoidance, collaborative environment mapping, and formation control etc. also require spatiotemporal information. Therefore, relative localization and clock synchronization have become pressing issues in the design and advancement of MASs.

Using external spatiotemporal reference is a practical solution. External reference options, such as the well-known Global Positioning System (GPS), optical motion capture systems, and the trendy ultra-wideband (UWB) anchors, have powered MASs for recreational or professional use [5]–[7]. Terrestrial wireless communications and the broadcast signals of opportunity (SOPs), such as cellular signals [8]–[11] and the signals from Iridium system [12], have also been demonstrated to navigate MASs in recent studies. In all cases, by comparing absolute position and time relative to the external reference, the relative localization and clock synchronization among each agent can be straightforwardly determined. However, such references require pre-installed infrastructures, which restricts the maneuverability of agents and are not always available or reliable in unknown environments.

To enable future multi-agent applications in any environment, relative localization and clock synchronization must rely on inter-agent measurements other than external references.
We notice that in the wireless sensor network (WSN) community, relative localization and clock synchronization are also necessary for spatiotemporal information acquisition in each sensor node for meaningful sensory data processing. Typically, the localization of sensor nodes requires inter-node ranging measurements. Regarding the ranging measurements, a popular choice is to use the time-of-arrival (TOA) metric, which relies on precise clock synchronization and time management. The clock synchronization is typically conducted in a two-way timing message exchange mechanism, which requires two-way TOA measurements between nodes \[14\]. Accordingly, the synergy between relative localization and clock synchronization is obvious. Various methods for joint localization and synchronization (JLAS) in WSN using TOA measurements have been proposed \[15\]–\[17\].

Indeed, a MAS can be treated as a mobile WSN, which motivates us to jointly perform relative localization and clock synchronization in MASs using the aforementioned methods in WSNs. However, the aforementioned methods are only suitable for static (or partially static) and sparse WSNs with low updating frequency requirements, which are difficult to apply to MASs. For MASs without external spatiotemporal reference support, we identify the additional three main challenges to the relative localization and clock synchronization problems:

1) **High-density.** MASs typically consist of dense small agents and act like swarms. Deriving two-way TOA measurements in a round-robin way for all agents is time and power consuming. Special considerations on communication protocol should be given in developing relative localization and clock synchronization methods, thus supporting theoretically unlimited agents simultaneously.

2) **High-maneuverability.** MASs are characterized by its high mobility and dynamics, e.g., with a maximum speed of 50 m/s. The collaboration control operations need high-frequency and real-time (e.g., 100 Hz) input of spatiotemporal information of all agents. However, conventional relative localization and clock synchronization methods in WSNs typically only provide one-shot estimates during a long period.

3) **SWaP constraints.** Last but not least, small agents usually come with size, weight, and power (SWaP) constraints, limiting their sensory payload and onboard resources for computation, signal processing, and communication.

To address all these challenges, we present BLAS, a precise, effective and reliable relative localization and clock synchronization system based on wireless broadcast architecture. The broadcast architecture is introduced to reduce the inter-agent communication overhead devoted to localization and synchronization in the networked MAS. Under the architecture, a MAS is categorized as parent and child agents as shown in Fig. 1. Parent agents act like moving beacons by periodically broadcasting wireless packets and child agents only passively receive the on-air packets. In BLAS, we first propose an asynchronous broadcasting and passively receiving (ABPR) communication protocol. The protocol serves two purposes: it schedules the broadcast of the parent agents using a distributed time division multiple access (D-TDMA) scheme and it also specifies the information embedded in broadcast packets, which is dedicated to joint relative localization and clock synchronization for both parent and child agents. Using the protocol, a two-way link can then be established between any pair of parent agents. We then present distributed state estimation approaches in parent agents to establish a moving spatiotemporal reference frame using the two-way packets. A distributed approach in child agents is also presented to jointly estimate the spatiotemporal states with respect to the pre-defined moving spatiotemporal reference, by only passively receiving the broadcast packets.

We note that BLAS only requires the broadcast packets to yield the inter-agent TOA measurements, thus can be considered as an enabling technique for MASs operating in any environment. The main contributions of this paper are summarized as follows:

- A novel wireless broadcast architecture based on which a relative localization and clock synchronization system is developed for dynamic and dense MASs with little resource requirements.
- A versatile communication protocol that simultaneously supports joint relative localization and clock synchronization for both parent and child agents.
- Real-time implementation of the system utilizing the off-the-shelf low-cost and light-weight hardware.

The rest of the paper is organized as follows. We first review the related literature on relative localization and clock synchronization in Section II. We then give our model formulations in Section III. In Section IV, we present our proposed ABPR protocol. We then present the joint relative localization and clock synchronization methods of parent agents and child agents in Section V and Section VI. Finally, simulations and real-world experiments are evaluated in Section VII and Section VIII. Section IX concludes the paper with comments on future works.
II. RELATED WORK

This section gives a concise review of related literature on relative localization and clock synchronization. These problems have been widely studied in various areas, including wireless sensor networks, robotics, and signal processing. The related scholarly works are extensive and hence we just focus on the most relevant papers.

A. Relative Localization

Relative localization refers to the problem of perceiving the position of other agents in the surroundings. The perception requires onboard sensors to provide inter-agent measurements. Numerous implementations have been developed utilizing different onboard sensors. According to the sensory modality, we can categorize these implementations into two groups: indirect and direct relative localization.

Indirect relative localization in MASs relies on optical sensors and/or laser scanners that can extract the environment-specific static features and landmarks. In these agents, the relative position is indirectly derived from observations of the same features and landmarks. For example, cameras are mounted in three unmanned aerial vehicles (UAVs) to identify the common objects in the environment, and the relative position between UAVs is calculated from these correspondences [18]. An alternative method exchanges the laser range scans between pairs of robots and determines the relative positions by estimating the overlap of their partial maps [19]. However, observation of the same scene is occasional and with great uncertainty. In the robotics community, the relative localization is always coupled with the environment mapping process, which leads to the multi-robot Simultaneous Localization and Mapping (SLAM) problem. The precise and continuous relative position estimates are derived by localizing the robots in a common global incremental map. Recent research has experimentally shown that multi-robot SLAM utilizing cameras [20] or laser scanners [21] can produce accurate relative position estimates. Such an approach builds on high-resolution cameras or high-quality laser scanners and on computationally expensive algorithms, such as smoothing [20] and particle filtering [21], to reduce uncertainty. Consequently, SLAM based relative localization requires heavy sensor payload and a powerful processor which is not always available on SWaP constrained agents.

Alternatively, direct relative localization is pursued using direct inter-agent measurements. For example, an audio-based approach directly perceives the neighbors by exploiting the direction and intensity of the sound emitted by its neighboring agents’ onboard piezo [22]. However, the accuracy is relatively low due to the sound noise of engines and/or propellers [23]. High-frequency-modulated infrared have been used to enable nearby agents to determine the relative position of the sender with a fast update rate [24], however, the relatively short operating range of a few meters is not suitable for large-scale environments. A vision-based approach detects the relative position of neighbors by recognizing the unique localization image patterns attached to neighboring agents [25]. However, the constraints specified by camera shutter frequency and field of view prevents its use for high dynamic agents. The natural weakness of visual methods is obvious at night or in light-changing environments. In all cases, the inter-agent measurements are derived between each pair of agents which produces redundancy and need more measuring time. Therefore, scalable implementations for high-density agents are impractical.

A much preferable approach for scalable relative localization is to communicate the inter-agent measurements through the networked MASs, to which we refer as mutual relative localization [26]. Hence, there is a need for MASs to establish a communication link between the agents as well as to produce inter-agent measurements. UWB is a promising sensory technology to endow MASs with the ability of simultaneous communication and range measuring [27], [28]. The fine temporal resolution and robustness to multipath enable reliable and precise direct inter-agent ranging measurements. Additionally, the advent of small, low-cost and low-power UWB transceiver chips makes it a suitable sensory choice for small SWaP constrained agents. To this end, our work builds on the UWB technology to realize mutual relative localization in MASs. To the best of our knowledge, no studies have demonstrated a UWB based mutual relative localization for high-density and high-maneuverability agents. Of particular relevance is the numerous works for the mutual relative localization of static agents in the WSN community [29], [30]. Closest in spirit to our approach is the work of “SHARP” [29], which first localized several reference nodes then localized the rest of the nodes with respect to the reference nodes. The difference between our work and the works in WSN is that our work deals with the dynamic agents with the assumption that all agents are in the UWB communication range of each other.

B. Clock Synchronization

In MASs, there is no global clock. Each agent has its own internal clock that reads its own time notion. Although they might be synchronized when they start, the frequency of the oscillators in each agent slightly differs from each other, thus leading to a drift in the notion of time. Clock synchronization has been widely investigated in wired networks, for example, the well-known Network Time Protocol (NTP) has been widely used for time synchronization on the Internet [32]. However, they are not suitable for wireless networked MASs which have potential motion, SWaP constraints and signal interference.

Clock synchronization is also a widely studied topic in the WSN community [14]. In WSNs, it can be achieved by sending a sequence of timing messages to the receiver sensors. The receiver sensors record the receiving time of the broadcasting messages and extract the embedded broadcast time information for synchronization processing. Generally, there are two different approaches according to the message transferring protocol: sender-receiver synchronization (SRS) and receiver-receiver synchronization (RRS). SRS is performed using the traditional two-way message exchange mechanism to synchronize the receivers with the sender, such as Romer’s protocol [33]. Instead of interacting with the
sender, RRS compares the receiving time of a same broadcast timing message among a set of receiving nodes to synchronize the receivers. A typical approach is the Reference-Broadcast Synchronization (RBS) [34]. However, to achieve network-wide synchronization, SRS and RRS approaches require a numerous number of timing messages, thus are time and power consuming, and increase communication overheads in dense networks. The Pairwise Broadcast Synchronization (PBS) is a promising way to reduce the overall consumption, which innovatively combines the RRS and SRS protocols [35]. In PBS, groups of nodes are synchronized by only passively receiving timing messages from parent nodes which perform a pairwise synchronization using SRS mechanism. This mainly motivates our work in this paper to tackle the high-density challenge of MASs. However, PBS assumes the distances between some nodes are known, which is not suitable for dynamic networks, e.g., networked MASs.

C. JLAS

The need to recover the distances between nodes for clock synchronization has driven the development of JLAS algorithms. As we have mentioned in the previous section, the distances can be recovered through TOA measurements, which require fine clock synchronization between nodes. Consequently, the distance based localization problem and the clock synchronization problem is highly related and can be jointly tackled. An early work [15] jointly solved the problems by first conducting clock synchronization and then localization using the same communication means, which is designed for static WSNs requiring low updating rate. Recently, JLAS have been solved simultaneously in one step. For example, a joint maximum likelihood estimator and a least squares (LS) estimator were proposed to determine the spatiotemporal information of an unknown sensor node with accurate anchors available, and a generalized total LS scheme is proposed with inaccurate anchors [56], however, they are computationally expensive. A low-complexity solution based on the linearized equations from TOA measurements and a weighted least square (WLS) criterion have proven to achieve a better estimation performance [57]. Approximately efficient and closed-form solutions were developed in [38]. However, all these methods require pre-installed static anchors with known positions and clock parameters. They have not yet been extended to the case with mobile anchors of unknown states.

An insightful JLAS approach considering unknown anchors’ states was proposed in [39]. It adopted a collaborative radio SLAM framework to simultaneously estimates the anchors’ states with the MASs’ states. Under the framework, each agent fused its onboard inertial information, GPS information, TOA measurements from anchors and inter-agent information from its neighboring agents to estimate all the states. In contrast to this fusion strategy, we choose to separately estimate the states of the mobile anchors (i.e., parent agents), and the states of each agent (i.e., child agent) using only UWB TOA measurements. In this way, the potential algorithm complexity improvement due to inter-agent information for a dense MAS can be eliminated.

Our proposed system can be treated like GPS in some aspects. ILAS in child agents using TOAs can be considered the same process in GPS user end, which was addressed using Bancroft algorithm [40]. However, Bancroft assumes the TOAs are measured concurrently, which is reasonable in GPS due to the code division multiple access (CDMA) scheme. For MASs utilizing TDMA scheme, the TOAs are measured consecutively. If the minor time difference between the consecutive TOAs are not taken into account during joint estimation, significant error can arise for high-maneuverability agents.

III. MODEL FORMULATION

A. Problem Statement

This paper studies the problem of relative localization and clock synchronization for a highly dynamic and dense MAS in unknown environments utilizing UWB technology. We focus on 2D space localization due to its practical advantages of easier implementation and experimental evaluation. Extension to 3D space of our proposed ideas is not difficult.

Suppose a MAS \( \mathcal{M} \) is composed of \( M \) mobile agents and is categorized into \( P \) parent agents and \( C \) child agents. Let \( \mathcal{P} = \{1, \cdots, P\} \) denotes the set of parent agents with unique identification indices and \( \mathcal{C} = \{P + 1, \cdots, P + C\} \) the set of child agents. The cardinality of the sets, i.e., \( P \) and \( C \) gives the total number of parent agents and child agents in the MAS, and \( \mathcal{M} = \mathcal{P} \cup \mathcal{C} \). Every agent is equipped with an UWB transceiver. For parent agents, the UWB transceiver is able to broadcast and receive UWB packets. For child agents, it only passively receives the on-air packets. We assume that the child agents are in the communication range of parent agents and the communication link between parent agents are available all the time. This is reasonable considering the maximum UWB communication range is relatively long and the topology size of swarmed MASs is relatively small. The goal of this paper is to real-time estimate the relative positions \( x_i(t) = [x_i, y_i]^T \) of agent \( i \in \mathcal{M} \) with respect to a reference coordinate attached to the reference agent \( j \) (usually \( j = 1 \)), as well as the relative clock parameters \( T_i(t), \omega_i(t) \) with respect to the reference agent.

B. Clock Model

Each UWB transceiver hosts an internal hardware clock, which is used to 1) timestamp the receiving and broadcasting event of UWB packets; 2) schedule the signal broadcasting; 3) synchronize the agents’ clock. Here we note that the clock synchronization between the agent and its UWB transceiver is addressed by a wired connection. For simplification, we refer the clock of an agent as the clock of the corresponding UWB transceiver. The clock value \( T_i(t) \) of an agent \( i \in \mathcal{M} \) is then read by counting the oscillations in the hardware clock oscillator which runs at a particular frequency, where \( t \) is the absolute reference time. For a perfect clock, \( T_i(t) = t \). However, the physical oscillators in each agent slightly differ from others due to environment changes, such as ambient temperatures and magnetic field, thus leading to frequency instabilities and the variation of clock value [41]. Using the
terminology in [42], we denote the clock offset of agent $i$ with respect to the perfect clock as $\omega_i^0(t)$, and the clock skew (the difference in the frequencies) of agent $i$ with respect to the perfect clock as $\omega_i^1(t)$. The clock value of agent $i$ is then given as

$$T_i(t) = t + \omega_i^0(t).$$

(1)

The agent clock parameters are given by $\mathbf{c}_i = [\omega_i^0, \omega_i^1]^T$, which consist of its clock offset and clock skew. The agent clock’s dynamics can be modeled as [43]

$$\mathbf{c}_i(t) = \mathbf{F}\mathbf{c}_i(t) + \mathbf{n}(t),$$

(2)

$$\mathbf{F} = \begin{bmatrix} 0 & 1 \\ 0 & 0 \end{bmatrix}, \quad \mathbf{n}_i = \begin{bmatrix} n_{T_i}^0 \\ n_{\omega_i}^0 \end{bmatrix},$$

where $n_{T_i}^0$ and $n_{\omega_i}^0$ are modeled as mutually independent zero-mean white noises. It is assumed that the collections of $\{n_{T_i}^0 | i \in N\}$ and $\{n_{\omega_i}^0 | i \in M\}$ are both independent and identically distributed with power spectra $S_{nT}$ and $S_{n\omega}$, respectively.

However, there is no global absolute time reference in MAASs, the clock offset and the clock skew of an agent cannot be measured. Typically, any agent’s clock can be chosen as a time reference, hence we only concern about the relative clock offset and relative clock skew. Therefore, we define the relative clock offset and clock skew of agent $i$ with respect to agent $j$ at time $t$, $\omega_{ij}^0(t)$ and $\omega_{ij}^1(t)$, respectively:

$$\omega_{ij}^0(t) = \omega_i^0(t) - \omega_j^0(t),$$

(3)

$$\omega_{ij}^1(t) = \omega_i^1(t) - \omega_j^1(t).$$

(4)

If agent $i$ and agent $j$ are perfectly synchronized, then we have: $\omega_{ij}^0(t) = 0$ and $\omega_{ij}^1(t) = 0$. It can be readily seen that the relative clock parameters evolve according to:

$$\mathbf{c}_{ij}^0(t) = \mathbf{F}\mathbf{c}_{ij}^0(t) + \mathbf{n}(t),$$

(5)

$$\mathbf{c}_{ij}^0 = \begin{bmatrix} T_j^i \\ \omega_{ij}^0 \end{bmatrix}, \quad \mathbf{n} = \begin{bmatrix} n_{T_j} \\ n_{\omega_{ij}} \end{bmatrix},$$

where $n_{T_j}$ and $n_{\omega_{ij}}$ are with power spectra $2S_{nT}$ and $2S_{n\omega}$, respectively.

C. Measurement Model

Consider an UWB packet broadcast from a parent agent $j \in P$ to an arbitrary agent $i \in M$, the broadcasting time $t_{tx}^{j\rightarrow i}$ and reception time $t_{rx}^{j\rightarrow i}$, both expressed in absolute time reference, are related by:

$$t_{tx}^{j\rightarrow i} = t_{tx}^{j\rightarrow i} + \tau_{ij}^1(t_{tx}),$$

(6)

where $\tau_{ij}^1(t_{tx})$ is the signal delay that can be characterized into several distinct parts:

$$\tau_{ij}^1(t_{tx}) = \tau_j + \tau_{ij}(t_{tx}) + \tau_i,$$

(7)

where $\tau_j$ is the broadcasting antenna delay of agent $j$, $\tau_i$ the receiving antenna delay of agent $i$, and $\tau_{ij}(t_{tx})$ the propagation delay. The antenna delays are constant and dependent on the antenna design, thus considered as a bias in the TOA measurement [44]. In this paper, we assume that they are deterministic and can be pre-calibrated. The propagation delay $\tau_{ij}(t)$ is given by:

$$\tau_{ij}(t) = \frac{d_{ij}(t)}{v_c},$$

where $v_c$ is the light speed, and $d_{ij}(t)$ is the distance between agent $i$ and $j$, $d_{ij}(t) = \| x_j(t) - x_i(t) \|$.

Typically, the reception time and broadcasting time are measured using individual agents’ internal clocks according to [1]. We measure the recorded broadcasting timestamp at agent $j$ and the reception timestamp at agent $i$ as $T_j(t_{tx}^{j\rightarrow i})$ and $T_i(t_{rx}^{j\rightarrow i})$, respectively. The TOA measurement is then given by:

$$\tau(t_{ix}^{j\rightarrow i}) = T_i(t_{tx}^{j\rightarrow i}) - T_j(t_{rx}^{j\rightarrow i}) + n_{ij}(t_{ix}^{j\rightarrow i}),$$

(8)

where $n_{ij}(t_{ix}^{j\rightarrow i})$ denotes the random delay caused by estimation errors on the stamping process, such as due to noise and multipath. The random delay is modeled as independent and identically distributed Gaussian noise [34], $n_{ij} \sim \mathcal{N}(0, \xi^2)$. Since the clocks between agents are not synchronized, using [1], [3], [2] and [6] the TOA measurement has the following form:

$$\tau(t_{ix}^{j\rightarrow i}) = T_i(t_{tx}^{j\rightarrow i}) + n_i(t_{tx}^{j\rightarrow i}) + \int_{t_{tx}^{j\rightarrow i}}^{t_{rx}^{j\rightarrow i}} T_i(t)dt + n_{ij}(t_{ix}^{j\rightarrow i}).$$

(9)

The first item of the equation corresponds to the relative clock offset between the broadcasting and the receiving agent at broadcasting time. The sum of following two items corresponds to the signal delay which is expressed in the agent $i$’s clock. Practically, the magnitude of the clock skew $\omega_i^0$ is unknown and can be up to $\pm 20$ parts per million (ppm) as the IEEE 802.15.4a standard indicates [45]. Consider the worst case $\omega_i^0$ of a constant 20 ppm over the propagation interval, the integration part is then approximately $2 \times 10^{-5}$, $\tau_i(t_{tx}^{j\rightarrow i})$, which is obviously much smaller than $\tau_i(t_{tx}^{j\rightarrow i})$. Consequently, by ignoring the integration term, we come to the following approximation of TOA measurement:

$$\tau(t_{ix}^{j\rightarrow i}) \approx T_i(t_{tx}^{j\rightarrow i}) + n_i(t_{tx}^{j\rightarrow i}) + n_{ij}(t_{ix}^{j\rightarrow i}).$$

(9)

At this point, we have shown that the TOA measurement is a function of the clock parameters and the physical relative positions of agents (correspond to the signal delay). Consequently, TOA measurements can be used for joint relative localization and clock synchronization.

IV. THE ABPR PROTOCOL

In our proposed BLAS system, the broadcasting of UWB packets is only performed by parent agents. All the remaining $M-1$ agents (including other parent agents and child agents) will receive the broadcast packets to derive the TOA measurements for state estimation. In order to support such an architecture, we employ an ABPR communication protocol, which schedules the broadcast of packets in parent agents and specifies a common packet format used for relative localization and clock synchronization in both parent and child agents.
A. D-TDMA scheduling

In order to achieve collision-free broadcasting of UWB packets between parent agents, the broadcasting is scheduled in a round-robin way as illustrated in Fig. 2. We employ a distributed time division multiple access (D-TDMA) scheduling scheme, which is implemented on individual parent agents to decide if and when to broadcast a packet. Fig. 3 shows a D-TDMA frame containing $P$ UWB packets. Typically, agents are allocated a predefined time slot for packet broadcasting [7]. However, the clocks between agents will drift in a long-running, thus leading to a collision of the predefined time slots. Consequently, it is necessary for the MAS to adjust the broadcasting time slots during operation. This is enabled through information exchange between agents in D-TDMA, which is summarized in Algorithm 1.

D-TDMA starts with an initialization procedure. Once powered on, parent agent $i$ will listen on the on-air packets for a specific while to see if any other parent agent already broadcasting. If no packets are received, it is the first one powered on, parent agent $i$ is the first one powered on (line 3). It then broadcasts a first packet (line 4) and determine the delay time $t_{delay}$ until next packet broadcasting (line 5). Straightforwardly, the delay time is determined by the multiplication of the number of parent agents and time slot intervals $\Delta t_s$, i.e., the time interval of a D-TDMA frame. Otherwise, it will receive a first packet from neighboring parent agents, and extract the identification of the broadcasting agent embedded in the packet (line 6). It then schedules its broadcasting according to the identifications (line 7-10). After initialization, subsequent adjustment procedure of D-TDMA adjusts the scheduled broadcasting delay upon receiving a packet. When parent agent $i$ broadcasts a packet according to scheduling, it immediately sets the broadcasting delay of the next packet (line 16). The broadcasting delay is then adjusted by comparing the broadcasting agent identifications (line 18-22). Note that, the adjustment is performed repeatedly on every packet reception (line 17). In this way, the broadcasting time slots of parent agents are allocated and adjusted in a global scope during run time.

Since the D-TDMA is performed in real time, parent agents may be inserted to or removed from the MAS during operation, making the system dynamically scalable and robust to failure. For example, when a new parent agent is inserted, it will first listen to the on-air UWB signals and then synchronize to the network to find an available time slot. If a time slot is available, it successfully joins the network and then begins to broadcast UWB packets. If no time slots are available, we can theoretically combine other channel access methods, such as frequency division multiple access (FDMA) to expand the capability of the UWB network.

Algorithm 1 D-TDMA Scheduling

1: let $i$ be an arbitrary parent agent.
2: procedure **INITIALIZATION**
3: \[\text{if } i \text{ is the first one powered on then} \]
4: \[\text{Broadcast a first packet.} \]
5: \[t_{delay} \leftarrow P \cdot \Delta t_s.\]
6: \[\text{else if} \text{ Receive a first packet from } j \in \mathcal{P} \setminus \{i\} \text{ then} \]
7: \[\text{if } j < i \text{ then} \]
8: \[t_{delay} \leftarrow (i - j) \cdot \Delta t_s.\]
9: \[\text{else if } j > i \text{ then} \]
10: \[t_{delay} \leftarrow (i + P - j) \cdot \Delta t_s.\]
11: \[\text{end if} \]
12: \[\text{end if} \]
13: **end procedure**
14: procedure **ADJUSTMENT**
15: Broadcast a packet according to scheduling.
16: \[t_{delay} \leftarrow P \cdot \Delta t_s.\]
17: \[\text{if} \text{ Receive a packet from } j \in \mathcal{P} \setminus \{i\} \text{ then} \]
18: \[\text{if } j < i \text{ then} \]
19: \[t_{delay} \leftarrow (i - j) \cdot \Delta t_s.\]
20: \[\text{else if } j > i \text{ then} \]
21: \[t_{delay} \leftarrow (i + P - j) \cdot \Delta t_s.\]
22: \[\text{end if} \]
23: \[\text{end if} \]
24: **end procedure**
B. Packet format

D-TDMA requires information of the broadcasting agent identification embedded in the packet. Furthermore, clock synchronization and relative localization also require information exchange between agents. To this end, we specify the packet format in Fig. 3. Each packet begins with a synchronization header consisting of ranging preamble and a start-of-frame delimiter (SFD), after which follow the PHY header (PHR), header consisting of ranging preamble and a start-of-frame exchange between agents. To this end, we specify the packet format as described in Section V-A.

We note that the relative position and local clock parameters are tracked between parent agents using the reported broadcasting timestamp, as described in Section V, and the states of child agents are determined using all the data contents, as described in Section VI. To this end, the specially designed packet format can be used for general purposes, which significantly reduces the communication overhead.

Given specific D-TDMA slot interval, the system broadcast rate is dependent on the number of parent agents, as the child agents only receive packets. In practice, we set the slot interval $\Delta t_s = 1$ ms, which is longer than the UWB packet length of approximate $0.3$ ms. By deploying $P = 10$ parent agents, we achieve a $100$ Hz broadcast rate. This enables a relatively high-frequency estimation of clock parameters and relative positions, which supports MASs with high maneuverability.

V. JLAS of Parent Agents

This section illustrates how parent agents can jointly track their relative positions and clock parameters using two-way broadcast packets. The JLAS is conducted in a two-step approach, which first performs clock synchronization and then relative localization. In contrast to [15], which adopts a similar two-step approach for static networks with low updating rate, we focus on the high-frequency and real-time estimation for parent agents.

We choose to track the local clock parameters for every parent agent using two-way TOA measurements. Further, we do not physically modify the internal clocks and just track the clock parameters to achieve virtual clock synchronization. This is in contrast to the standard clock synchronization approaches, which aim to achieve optimal global clock parameters and synchronize every clock to this optimal global reference. In practice, we implement the clock synchronization algorithms in a distributed way. Every parent agent locally holds multiple Kalman filters to track the pairwise pseudo-clock parameters with respect to other parent agents. This enables high-frequency and real-time clock parameter estimation. After two-way synchronization completion, the two-way range between a pair of parent agents can be derived in one round, i.e., in one D-TDMA frame, which is a relatively short time, e.g., $10$ ms, the motion of parent agents is negligible and the range between parent agents remains constant. We can then recover the topology of parent agents from inter-agent ranges with $100$ Hz frequency.

A. Distributed clock synchronization in parent agents

Since the parent agents are dynamic, the propagation delay $\tau$ is not deterministic. As we can see from (9), the relative clock parameters are then not observable using only one-way TOA measurements. Therefore, we propose to track the pseudo-clock parameters which consist of the relative clock parameters and the propagation delay in the parent agent’s local perspective.

Without loss of generality, we discuss the case of an arbitrary parent agent $i \in P$ synchronizing to its neighboring parent agents $P \setminus \{i\}$. The local clock parameters to be estimated are defined as $C_i = [C_i^1, \cdots, C_i^n]$, and $C_i^j$ are the pseudo-clock parameters of $i$ with respect to $j$:

$$C_i^j = [\tilde{T}_i^j, \omega_i^j],$$

where

$$\tilde{T}_i^j = T_i^j + \tau_i^j,$$

(10)

is the pseudo-clock offset and $\omega_i^j$ is clock skew of $i$. For each $C_i^j$, we establish a Kalman filter. Under the assumption that the motion of parent agents is negligible in a small interval ($10$ ms), the Kalman filter linear dynamic model is given using (5):

$$\dot{C}_i^j(t) = FC_i^j(t) + n(t).$$

Further, the states are observed upon the reception of an UWB packet by $i$, with the Jacobian matrix $H$ defined with respect to the state as $H = [1 \ 0]$.

Algorithm 2 outlines the recursive state estimation steps for parent agent synchronization using discrete-time Kalman filters. This algorithm is implemented in each parent agent. During initialization, a number of $P - 1$ Kalman filters are established (line 1-3). Upon reception of an UWB packet, the parent agent reads the broadcasting agent id and extract the TOA measurement (line 6-7). Then it switches into the corresponding Kalman filter process and calculates the discrete reception time interval (line 8). The Kalman filter state and covariance matrix is then propagated (line 10) and updated using the TOA measurement (line 11), where the discrete-time noise covariance matrix is given by

$$Q = \begin{bmatrix}
S_{n_x} \Delta t + 2S_{n_x} \frac{\Delta t^2}{3} & S_{n_x} \Delta t \\
S_{n_x} \Delta t^2 & S_{n_x} \Delta t^2
\end{bmatrix}.$$

During implementation, we also set thresholds for the values of the estimation error covariance matrix to detect whether a parent agent have left the network. The covariance grows if no UWB packets are received from the left parent agents, and if it exceeds the thresholds, the associated clock parameters will not be embedded in the broadcast packet.
Algorithm 2 Distributed clock synchronization in parents

1: let $i$ be an arbitrary parent agent.
2: for $j \in \mathcal{P} \setminus \{i\}$ do
3: Initialize $j$th Kalman filter with initial state $C_{i,0}^j$ and initial state error covariance matrix $P_{i,0}^j$.
4: end for
5: while system running do
6: Receive the $k$th packet from agent $j \in \mathcal{P} \setminus \{i\}$.
7: Extract the TOA measurement: $(\xi, \tau_i^j)$. 
8: Calculate the reception interval: $\Delta t = T_{rx,k}^j - T_{tx,k-1}^j$.
9: Compute the discrete-time state transition matrix: $F = I_2 + \Delta t F$.
10: Propagate the $j$th Kalman filter:
\[C_{i,k}^j \leftarrow F C_{i,k-1}^j, \quad P_{i,k}^j \leftarrow F P_{i,k-1}^j F^T + Q.\]
11: Update the $j$th Kalman filter using TOA $\tau_k^j$:
\[K = P_{i,k}^j H^T (H P_{i,k}^j H^T + \xi^2)^{-1}, \quad C_{i,k}^j \leftarrow C_{i,k}^j + K (\tau_k^j - \bar{T}_{i,k}^j), \quad P_{i,k}^j \leftarrow (I_2 - KH) P_{i,k}^j.\]
12: end while

B. Inter-agent range estimation in parent agents

When the local clock parameters are acquired in parent agents, the inter-agent range can be estimated from the exchanging packets. Consider a pair of parent agents $i$ and $j$, $(i < j)$ as illustrated in Fig. 3, parent agent $i$ first broadcasts an UWB packet and then receives one from parent agent $j$ in one D-TDMA frame interval. The relative clock offset of $i$ with respect to $j$ at broadcasting time $t_{tx}^j$, $T_i^j(t_{tx}^j)$ is given by (8):
\[T_i^j(t_{tx}^j) = T_i(t_{tx}^j) - T_j(t_{tx}^j) = -T_j^i(t_{tx}^j),\]
which is the negative of relative clock offset $T_j^i(t_{tx}^j)$ of $j$ with respect to $i$ at the same time. Using (10), $\tau_i^j$ can be written in terms of the pseudo-clock offset estimated respectively in $i$ and $j$ as:
\[\tau_i^j(t_{tx}^j) = \frac{1}{2} (T_j^i(t_{tx}^j) + \bar{T}_i^j(t_{tx}^j)).\]  

(11)

However, this requires parent agent $i$ and $j$ broadcast a packet at the same time to estimate the corresponding pseudo-clock parameters and exchange them without latency, which is impractical for D-TDMA scheduling scheme. Therefore, we choose to propagate the pseudo-clock parameters in agent $j$ until broadcasting as an approximation of $T_j^i(t_{tx}^j)$:
\[\bar{T}_j^i(t_{tx}^j) \approx T_j^i(t_{tx}^j) + \Delta t \cdot \omega_j^i(t_{tx}^j),\]
where $\Delta t = T_j(t_{tx}^j) - T_j(t_{tx}^j) \approx (j - i) \cdot \Delta t$. This is the main reason why we embed the propagated pseudo-clock parameters in the UWB packets as the aforementioned protocol.

To this end, after reception of an UWB packet from $j$, the parent agent $i$ can estimate the pseudo-clock offset $T_j^i(t_{tx}^j)$ and extract the embedded pseudo-clock offset $\bar{T}_j^i(t_{tx}^j)$, the inter-agent range can then be estimated using (11):
\[d_j^i(t_{tx}^j) = v_c \left( \frac{T_i^j(t_{tx}^j) + \bar{T}_i^j(t_{tx}^j) - \tau_i - \tau_j}{2} \right).\]  

(12)

We note that the distance is estimated using two-way packets in one round, i.e., in one D-TDMA frame. Even with the case of packet loss, for example, the $k$th packet from $i$ to $j$ is lost, parent agent $i$ can still estimate the distance as long as it receives the $k$th packet from $j$ to $i$. Since we can propagate $T_j^i(t_{tx}^j)$ according to $\Delta t$ (though with increasing uncertainty). Also we note that the inter-agent ranges are estimated in a distributed way. Each parent agent is able to track the pair-wise distances between parent agents: $\{d_j^i \mid i \in \mathcal{P}, j \in \mathcal{P}, i \neq j\}$. Since they are aware of the pair-wise clock parameters by receiving the broadcast UWB packets. Consequently, a distributed relative localization algorithm in parent agents can be achieved.

C. Relative localization in parent agents

If the inter-agent ranges are known for each pair of parent agents, the topology of parent agents can be recovered. In other words, the relative positions of each parent agents can be estimated. In the context of WSN localization, given the inter-agent range measurements, a configuration of the sensor positions can be estimated using the classical MDS method. A distributed implementation of MDS can be found in [49]. However, high-maneuverability MASs are with varying topology, thus requiring real-time and high-frequency relative localization. Further, SWaP constrained agents pose additional...
requirement on the complexity of localization algorithms. Therefore, in the context of dynamic MASs, it is often hard to adapt the MDS method, which requires many computation resources to minimize a rather complex cost function.

To this end, we choose to determine the topology by assuming that the parent agents 1, 2, 3 can uniquely construct a 2D reference Cartesian coordinate. The origin of the coordinate is set as the position of agent 1, positive x-axis along the parent agent 2, and positive y-axis in the direction of parent agent 3. The rest of parent agents can then determine their positions relative to this coordinate using the range measurements with respect to the first three parent agents and the broadcast information of parent agents’ positions. In this way, the initial relative position of parent agents can be given in closed-form as:

\[
x_1 = \begin{bmatrix} 0 \\ 0 \end{bmatrix}^T, \\
x_2 = \begin{bmatrix} d_{21} \\ 0 \end{bmatrix}^T, \\
x_i = \begin{bmatrix} d_{12}^2 + d_{13}^2 - d_{23}^2 \\ 2d_{21}d_{23} \end{bmatrix}^T, i = 3, \cdots, P,
\]

where the y coordinate of parent agent 3 is set to be positive and the sign of y-coordinates of other parent agents is determined by comparing their distance to parent agent 3.

We then use all the mutual distance measurements to refine the initial results. We seek to distribute the relative position \(x_i\) for parent agent \(i\) by minimizing the following local cost function:

\[
S(x_i) = \frac{1}{2} \sum_{j \in P \setminus \{i\}} (d^{ij} - \|x_j - x_i\|)^2,
\]

where the distance \(d^{ij}\) and the position \(x_j\) of its neighboring parent agents are extracted from the received UWB packets. The optimization problem is solved using an iteratively least squares method under the constraints of \(x_1 = 0, y_1 = 0, y_2 = 0\).

We note that the accuracy of the relative position estimate is highly related to the inter-agent range accuracy. Since we do not have access to global position and orientation or the odometry information over time, we can only determine a rough topology of parent agents in local perspective. Future improvements to obtain more precise and smooth relative position of parent agents would be possible by utilizing additional sensors, such as cameras and inertial measurement units (IMUs). Then by fusing with inter-agent range measurements, the parent agents can act like moving beacons broadcasting UWB packets with their absolute and smooth positions embedded. This is beyond the scope of this paper and left as our future work.

VI. JLAS OF CHILD AGENTS

Along with the synchronized clocks in parent agents, the spatiotemporal reference is then obtained in a high frequency and real-time embedded in the broadcast UWB packets. Upon passively receiving the broadcast packets, our aim is to estimate the state of the child agents \(c \in C\):

\[
X^i_c = [T^i_c(t^{i-c}_{1x}), \omega^i_c(t^{i-c}_{1x}), \hat{x}_c(t^{i-c}_{1x})],
\]

which consists of the relative clock parameters with respect to a reference parent agent \(i\) and the relative position.

We choose to utilize an iterative least squares estimator for joint estimation using the TOA measurements. However, the joint estimation faces two problems. One lies in the D-TDMA scheduling scheme, which leads to asynchronous TOA measurements (see Fig. 2). The other lies in the virtual clock synchronization in parent agents, which leads to the TOAs measured with respect to different time references.

Before diving into the estimator, we first investigate the observation equation. Consider one round of UWB broadcasting from parent agents, i.e., one D-TDMA frame, the TOA measurements at child agent \(c\) are then given by a sequence:

\[
\{\tau(t^{1-c}_{1x}), \tau(t^{2-c}_{1x}), \cdots, \tau(t^{P-c}_{1x})\}.
\]

Consider the TOA measurement from parent agents \(j\)

\[
\tau(t^{j-c}_{1x}) = T^i_c(t^{j-c}_{1x}) + \tau^i_c(t^{j-c}_{1x}) + n^j_c.
\]

We choose an arbitrary reference parent agent \(i\). From [3], we have:

\[
T^i_c(t^{j-c}_{1x}) = T^i_c(t^{i-c}_{1x}) + T^j_i(t^{i-c}_{1x}) \\
\approx T^i_c(t^{i-c}_{1x}) + \omega^i_c(t^{i-c}_{1x}) \cdot \Delta t + T^j_i(t^{i-c}_{1x}),
\]

where \(\Delta t = T^j_i(t^{j-i}_{1x}) - T^j_i(t^{j-c}_{1x}) \approx (j-i) \cdot \Delta t_i\). From [7], we have:

\[
\tau^i_c(t^{j-c}_{1x}) = \tau_j + \tau_c + \frac{\|x_j(t^{i-c}_{1x}) - x_c(t^{i-c}_{1x})\|}{v_c}.
\]

The TOA measurement from parent agent \(j\) can then be rewritten as:

\[
\tau(t^{j-c}_{1x}) = T^i_c(t^{j-c}_{1x}) + \omega^i_c(t^{j-c}_{1x}) \cdot \Delta t + T^j_i(t^{i-c}_{1x}) \\
+ \tau_j + \tau_c + \frac{\|x_j(t^{i-c}_{1x}) - x_c(t^{i-c}_{1x})\|}{v_c} + n^j_c.\]

As we can see, the state of child agent can be observed. We note \(\Delta t\) corresponds to the aforementioned asynchronous TOA problem, and \(T^j_i(t^{j-c}_{1x})\) corresponds to the virtual clock synchronization problem. If these items are not carefully considered, the estimation results will be incorrect.

We now try to recover the relative clock offset \(T^j_i(t^{j-c}_{1x})\) from the local clock parameters extracted from the consecutive UWB packets. From (10), we arrive at:

\[
T^j_i(t^{j-c}_{1x}) = \frac{\overline{T}^j_i(t^{j-c}_{1x}) - \overline{T}^j_i(t^{j-i}_{1x})}{2} \\
\approx \frac{\overline{T}^j_i(t^{j-c}_{1x}) + \omega^j_i(t^{j-c}_{1x}) \cdot \Delta t) - \overline{T}^j_i(t^{j-i}_{1x})}{2},
\]

where the pseudo-clock parameters in the second line equation are embedded in UWB packets. In practice, \(T^j_i(t^{j-c}_{1x})\) can also be derived from other pairs of relative clock parameters:

\[
T^m,i_{i,m}(t^{i-c}_{1x}) = T^m_i(t^{i-c}_{1x}) + T^m_m(t^{i-c}_{1x}),
\]

where \(T^m_i(t^{i-c}_{1x})\) and \(T^m_m(t^{i-c}_{1x})\) are computed from the corresponding pseudo-relative clock parameters, \(m \in P \setminus \{i, j\}\). In this way, the relative clock offset can be refined by averaging:

\[
T^j_i(t^{j-c}_{1x}) \leftarrow \frac{T^j_i(t^{j-c}_{1x}) + \sum_{m \in P \setminus \{i,j\}} T^m,i_{i,m}(t^{i-c}_{1x})}{P - 1}.
\]
To the end, we can obtain the pseudo-range observation equation by multiplying light speed with (13):
\[
h_j(X^i_i) = v_c \cdot (T^i_i(t^c_{ix}^i) + \omega_c^i(t^c_{ix}^i) \cdot \Delta t + T^j_j(t^c_{ix}^j) + \tau_j + \tau_c) + \|X^i_i(t^c_{ix}^i) - X^j_j(t^c_{ix}^j)\| + v_c \cdot n^{ij}.
\]

Algorithm 3 JLAS for child agents
1: let \( c \in C \) be an arbitrary child agent.
2: \textbf{while} Received a D-TDMA UWB frame \textbf{do}
3: Get TOA measurements sequence \( \{\tau(t^c_{ix}) \mid j \in P\} \): \[\Box\].
4: Recover pseudo-range measurements \( \{\rho_j \mid j \in P\} \):
\[
\rho_j = v_c \cdot \tau(t^c_{ix}).
\]
5: Extract the broadcast local clock parameters sequence \( \{C_j(t^c_{ix}) \mid j \in P\} \).
6: Extract position of parent agents \( \{x_j \mid j \in P\} \).
7: Get relative clock offset sequence \( \{T^j_j(t^c_{ix}) \mid j \in P\} \): \[\Box\].
8: Iteratively solve for \( \tilde{X}^i_i \):
\[
\text{arg min } S(\tilde{X}^i_i) := \sum_{j \in P} \|\rho_j - h_j(X^j_j)\|^2.
\]
9: \textbf{end while}

Algorithm 3 outlines the JLAS of child agents. Without loss of generality, we let reference parent agent \( i = 1 \). By stacking all the pseudo-range measurements, we can form a least squares problem and iteratively solve it to jointly estimate the child agent’s state.

VII. SIMULATIONS

In this section, we demonstrate the performance of our proposed JLAS algorithm for fully dynamic MASs in numerical simulations. The simulation configuration is given first, the results are then provided.

1) Simulation setup: The simulated scenario of a MAS consisting of 5 parent agents and 3 child agents, labeled with their identification indices as 1, \( \cdots \), 8, is illustrated in Fig. 5. We preallocate 5 time slots with a slot interval \( \Delta t_s = 0.001 \) s. The initial clock offset \( t_{i,0}^{0} \) and initial clock skew \( \omega_{i,0}^{0} \) of each agent \( i \) are set as random variables, which have continuous uniform distributions, \( t_{i,0}^{0} \sim U(-5 \times 10^{-7}, 5 \times 10^{-7}) \) s and \( \omega_{i,0}^{0} \sim U(-5, 5) \) ppm. The dynamics of the clock of each agent are then simulated using \[\Box\]. To simplify the comparison of simulation results with ground truth trajectories, parent agent 1 is set to be static at \((0, 0)\) m and parent agent 2 is set to move along the x-axis, therefore the process of trajectory alignment can be ignored. We note that this setup does not have any implication on the simulations, since we focus on the relative localization with respect to the reference coordinate rigidly attached to parent agent 1. The eight agents are initially located at \((0, 0)\), \((40, 0)\), \((40, 56.4)\), \((13, 42.5)\), \((50, 15)\), \((32.8, 25)\), \((2, 30)\) and \((40, 20)\) m. The temporal precision of TOA measurements is associated with the noise \( n^{ij} \) in \[\Box\] with standard deviation \( \xi \). We set \( \xi = 1.5 \times 10^{-10} \) s, which is equivalent to a spatial precision of 0.045 m. The antenna delays and the channel imperfections, such as non-line-of-sight (NLOS) effects, are not considered here. The initial estimation covariance matrices of the Kalman filters for clock synchronization in parent agents are set as \( P_{i,0}^{j} = \text{diag}[0.1, 1] \). The simulation time length is set to be 60 s. The simulation configurations are summarized in Table I.

2) Simulation results and discussion: We first demonstrate the clock synchronization results and then the relative localization results. Without loss of generality, we set parent agent 1 as a reference agent. Fig. 6 shows the estimation error of pseudo-clock parameters \( C^i_i \) calculated on parent agent \( i \), \( i = 2, \cdots, 5 \). The statistical results of the clock synchronization errors are presented in Table II. The root-mean-square error (RMSE) and standard deviation values of the synchronization errors prove the effectiveness and good performance of our proposed algorithm. Note that the synchronization results between other pairs of parent agents, namely \( C^j_j \) for \( i \in P, j \in P, i \neq j \), behave similarly to \( C^1_1 \). Fig. 7 illustrates the clock synchronization results in child agents. The statistical results of the results are summarized in Table III. Consider that the actual clock offset can be up to approximately \( 10^{-6} \) s for the worst case according to the simulation configurations in Table I, the average clock offset error of 0.21 ns thus provides an accuracy of one ten

| Parameter | Value | Unit |
|-----------|-------|------|
| \( P \)   | 5     | -    |
| \( C \)   | 3     | -    |
| \( \Delta t_s \) | 0.001 | s    |
| \( S_{\nu T} \) | \( 4.7 \times 10^{-20} \) | s    |
| \( S_{\nu \omega} \) | \( 7.5 \times 10^{-20} \) | s\(^{-1}\) |
| \( \xi \) | \( 1.5 \times 10^{-10} \) | s    |
| \( t_{i,0}^{0} \) | \( U(-5 \times 10^{-7}, 5 \times 10^{-7}) \) | s    |
| \( \omega_{i,0}^{0} \) | \( U(-5, 5) \) | ppm  |
We note that the synchronization results in child agents are worse than those in parent agents. This comes from the error propagated from the parent agents, since child agents only passively receive the broadcast information with uncertainty and have no means to observe it.

We then investigate the relative localization errors. The relative localization errors of parent agents and child agents are plotted in Fig. 8. The statistical results are provided in Table III. It is easy to see that our proposed method can effectively estimate the relative positions of the dynamic agents with estimation errors bounded by approximately 0.12 m.

Considering 5 time slots with slot interval of $\Delta t_s = 1$ ms allocated in our simulations, the estimation frequency is then 200 Hz, which is sufficient for collaboration or data fusion of a MAS in most scenarios. We also note that the agents move at a typical average speed of 1 m/s and the number of child agents can be theoretically unlimited. To summarize, our BLAS can effectively solve the JLAS problem for a fully dynamic MAS with high density.

Finally, we would like to discuss the convergence and potential degradation of our BLAS algorithms in the presence of antenna delays and NLOS signals. We first discuss the effect of antenna delays. For parent agents, they will not prevent the convergence of the clock synchronization algorithms, since they are deterministic parameters. If they are not considered and not calibrated, they will be treated as additional pseudo-clock offsets between parent agents. This will pose a significant bias in inter-agent range estimation, thus the relative localization algorithm will diverge. For child agents, they will not prevent the convergence of the JLAS. As we have mentioned before, the delays serve as pseudo-clock offsets, thus only leading to an estimation bias on the relative clock offset of the child agent. In our practical implementation, the antenna delays are pre-calibrated and compensated. We then discuss the effects of NLOS. NLOS will prevent the convergence of the JLAS both in parent and child agents. NLOS can be considered as observation outlier as it diverges from measurement model assumptions, which introduces a positive bias in range that leads to divergence of the algorithms. We note that in our dense MAS scenario, NLOS between agents typically occurs due to the occlusions of other agents. A MAS with controlled maneuverability has the potential to avoid these NLOS situations. Additionally, since we have a high estimation frequency, fusion with additional sensors such as IMUs will give access to NLOS identification and mitigation. NLOS avoidance, identification and mitigation is another broad research topic which is out of the scope of this paper and left as our future work.

VIII. EVALUATION

In this section, we perform two experiments to evaluate the proposed BLAS system. In the first experiment, we evaluate the performance of the proposed algorithm for dynamic parent agents. After the spatiotemporal reference is determined by parent agents, we then perform an experiment to illustrate that our system supports theoretically unlimited child agents. We also show that child agents are able to accurately localize themselves in real-time and high-frequency.

![Fig. 6. Synchronization results in parent agents. (a) Evolution of pseudo-clock offset error estimated in parent agent $i$, $i = 2, \cdots, 5$. (b) Evolution of clock skew error estimated in parent agent $i$, $i = 2, \cdots, 5$.](image)

![Fig. 7. Synchronization results in child agents. (a) Evolution of clock offset error estimated in child agent $i$, $i = 6, 7, 8$. (b) Evolution of clock skew error estimated in child agent $i$, $i = 6, 7, 8$.](image)
TABLE II
STATISTICS OF JLAS ERRORS

| Agent | (Pseudo-)clock offset (ns) | Clock skew ($1 \times 10^{-3}$ ppm) | Relative position (cm) |
|-------|---------------------------|----------------------------------|----------------------|
|       |                           | [RMSE, standard deviation]       |                      |
| 2     | [0.16, 0.11]              | [5.0, 3.2]                       | [0.9, 0.6]           |
| 3     | [0.18, 0.10]              | [5.8, 3.4]                       | [2.7, 2.1]           |
| 4     | [0.16, 0.09]              | [5.8, 3.6]                       | [2.4, 1.6]           |
| 5     | [0.17, 0.11]              | [5.1, 3.2]                       | [2.1, 1.5]           |
| 6     | [0.26, 0.09]              | [139.9, 87.9]                    | [10.8, 5.7]          |
| 7     | [0.29, 0.18]              | [144.2, 89.2]                    | [11.4, 6.1]          |
| 8     | [0.27, 0.17]              | [151.5, 94.4]                    | [10.9, 5.8]          |

Fig. 8. Relative localization results. (a) Evolution of relative localization error estimated in parent agent $i$, $i = 2, \cdots, 5$. (b) Evolution of relative localization error estimated in child agent $i$, $i = 6, 7, 8$.

A. Implementation

We implement our algorithms on the STM32F427 ARM chip, which controls a DecaWave DW1000 UWB module. Fig. 9 shows the hardware setup used in our experiments. Though we categorize a MAS into parent and child agents, they are equipped with the same hardware setup and operate as a homogeneous team. In this way, a MAS can quickly respond to the failure of a single agent by replacing it with a homogeneous one. Further, our setup requires little payload capability and onboard resources. The D-TDMA frame has a length of 10 ms and contains 10 time slots allocated for ten parent agents. This enables 100 Hz UWB packet broadcasting and thus a 100 Hz estimation frequency.

B. Parent agent experiments

As we have no ground truth for the clock parameters, we choose to evaluate the quality of the ranging results due to the coupling between clock synchronization and ranging. We ignore the evaluation of relative localization results since accurate ranging results yield accurate localization results in our relative localization algorithm.

1) Setup: We equip three parent agents with our UWB hardwares, as shown in Fig. 10a. One of the parent agents is an unmanned ground vehicle (UGV) that is manually controlled to randomly move in a rectangular area of 2.5 m $\times$ 4 m, with a maximum velocity of 0.25 m/s. The rest of them are set as static parent agents. For performance comparison, the UGV is equipped with a LiDAR and a LiDAR map of the environment is established in advance. The UGV’s position is then tracked by finding the correspondences to the map with a frequency of 2 Hz. The standard deviation of the 2D ground truth position error is approximately 0.05 m. Since the static agents are represented as obstacles in the LiDAR map, their positions are then directly obtained by querying the map. Fig. 10b illustrates the topology of the parent agents and the output trajectory of the UGV. In this way, by logging the output positions, we can obtain the real-time distance between parent agents, which is collected as ground truth. Further, the UGV is time synchronized with the static agents by our hardware setup sending one-pulse-per-second (1PPS) timing packets.

We then utilize a virtual parent agent, which only receives the broadcast UWB packets but runs a distributed inter-agent range estimator at 100 Hz. The distances between the three parent agents are real-time logged to a PC for evaluation. They are linearly fitted to the ground truth to calibrate the bias caused by antenna delays in (12).

2) Results: Fig. 11 illustrates the inter-agent ranging results for three parent agents. As we can see, the estimated range is quite close to the ground truth. Note that the repetitive large range noise in Fig. 11c is caused by the NLOS effects, in which case the UGV moves through the line connecting...
Fig. 10. (a) Three parent agents equipped with our UWB hardwares. (b) The topology of the parent agents and the trajectory of the UGV obtained using a LiDAR sensor.

two static parent agents (see Fig. 10b). The ranging error is demonstrated in Fig. 12. In terms of RMSE, the ranging results of our method yields an average accuracy of 0.051 m and the associated standard deviation is 0.050 m. The ranging accuracy corresponds to a clock synchronization accuracy of about 0.172 ns, which satisfies the synchronization requirements for most MASs.

C. Child agent experiments

Previous experiments have shown good quality of the ranging results. Consequently, good clock synchronization and relative localization results are obtained, and a spatiotemporal reference is then established. To demonstrate that the JLAS of child agents is also applicable to dense, dynamic and real-time child agents, we utilize four static parent agents to establish a static spatiotemporal reference. For any number of child agents, we then try to synchronize to and localize against the spatiotemporal reference. Since the clock parameters have no ground truth, we focus to evaluate the localization performance.

1) Setup: Four static parent agents are set on flat ground with the same heights. They form an approximate 5 m × 7 m rectangular, and their relative positions are post-processed using their inter-agent ranging results. Two child agents are mounted on the two ends of a turntable within the rectangular formed by parent agents, as illustrated in Fig. 15. The turntable has a diameter of 1.733 m, and rotate at an average angular velocity of 0.14 rad/s. The two child agents then move with a linear velocity of 0.12 m/s and localize themselves by only receiving the UWB packets. The localization results are real-time logged to a host computer for evaluation. Since we have no ground truth of child agent positions, we use the error of distance between two child agents as main evaluation metric. The distance is calculated using the estimated localization results.

2) Results: Fig. 14 shows the relative localization results for two child agents. In Fig. 14a, the blue and green dotted lines indicate the estimated positions which are circular. Since the child agents are rigidly mounted on the two ends of the turntable, the coincident of the trajectories provides strong qualitative evidence of the algorithm’s performance in accuracy and consistency. Fig. 14b and 14c illustrate the estimated x y positions, which are sinusoidal forms and present exact correspondence of the circular trajectories. The distance between the two child agents are then calculated using the estimated localization results, and the distance error is illustrated in Fig. 15. The RMSE and the associated standard deviation of the calculated distance is 0.064 m and 0.048 m. The distance error appears to be dependent on the positions of the child agents. As we observe a relatively strong correlation between the repeatability of a bias on the order of 0.1 m contained in distance error and the circular pattern of movements for child agents. The bias is a determined value, thus can be calibrated in future works. The main cause of the bias can be explained by the relative position and orientation between UWB antennas.

D. Discussion

The experimental results for parent and child agents together show that we can obtain accurate and real-time relative localization results for a MAS. A typical nanosecond accuracy for clock synchronization can be achieved. For high-density MASs containing a number of agents, we can choose a small set of them as parent agents performing packet broadcasting, as described in our broadcast architecture. Our APBR protocol ensures the collision-free broadcasting, thus enabling efficient information sharing in parent agents to establish a real-time updated spatiotemporal reference, as shown in the parent agent experimental results. The rest of the agents are then set as child agents that only receive the broadcast packets. In this way, the system can simultaneously support theoretically an unlimited number of child agents. The child agent experiments have shown that we can real-time and accurately localize the child agents against the spatiotemporal reference using the received packets. Though we only show the results for two child agents, the extension to any number of child agents is straightforward if the NLOS effects can be neglected. In our experiments, the broadcasting frequency is set as 100 Hz. As our protocol supports JLAS of child and parent agents using the same broadcast packets and our estimation approaches are distributely implemented, the estimation frequency for both child and parent agents is then 100 Hz. Therefore, our
Fig. 11. The inter-agent ranging results for each pair of parent agents. The red solid line indicates the estimation results while the blue solid line indicates the ground truth. (a) The range between parent agent $0$ and $1$, $d_{01}$. (b) The range between parent agent $0$ and $2$, $d_{02}$. (c) The range between parent agent $1$ and $2$, $d_{12}$.

Fig. 12. The error of inter-agent range for each pair of parent agents. (a) Parent agent $0$ and $1$. (b) Parent agent $0$ and $2$. (c) Parent agent $1$ and $2$. The average ranging error is 0.051 m.

Fig. 13. The topology of the agents in our experiments. Four static parent agents are set on ground (red) and two child agents are mounted on the two ends of a turntable (blue and green).

The system can also be applied to high-maneuverability MASs which require real-time and high-frequency spatiotemporal state estimation. Further, our system is developed into a stand-alone measurement unit with low weight, small volume and low power consumption, thus can be integrated into SWaP constrained MASs. To this end, our proposed BLAS system is proven feasible to be applied to high-density, high-maneuverability and SWaP constraint characteristics. A broadcast architecture and the supporting approaches, such as an ABPR communication protocol and distributed parent-child state estimators have been presented and implemented in our system. Simulation and experimental results verified that the proposed BLAS system is capable of establishing accurate and high-frequency relative localization and clock synchronization for dynamic dense MASs with limited resources.

Remark Comparisons between our BLAS with the state-of-arts are not straightforward, since the previous relevant methods are not specially designed for a dynamic and dense MAS in an infrastructure-free environment as we have discussed in Section II. To the best of our knowledge, we are the first to address the JLAS problem for such a MAS using a broadcast UWB architecture.

IX. Conclusion

In this paper, we present a wireless broadcast relative localization and clock synchronization system for MASs with high-density, high-maneuverability and SWaP constraint characteristics. A broadcast architecture and the supporting approaches, such as an ABPR communication protocol and distributed parent-child state estimators have been presented and implemented in our system. Simulation and experimental results verified that the proposed BLAS system is capable of establishing accurate and high-frequency relative localization and clock synchronization for dynamic dense MASs with limited resources.

The proposed system can be applied to a number of scenarios, e.g., establishing a UAV Ad-Hoc network, in which parent agents can output real-time topology and clock parameters of the dynamic network to aid network routing. Additionally, although this study focuses on the localization results which are relative, it can be extended to obtain absolute localization for MASs. In that case, our BLAS system can be used as a sensory system, which yields ranging measurements between parent agents. By utilizing other proprioceptive sensors, such as cameras, LiDARs or IMUs, we can utilize collaborative localization algorithms to establish absolute spatiotemporal references in parent agents. The parent agents can then serve like pseudo-GPS satellites, which enables any number of users (child agents) to retrieve their spatiotemporal information in unknown environments.

As part of future work, we will extend the proposed BLAS to 3D space and include more extensive evaluation of the proposed methods.
Fig. 14. Localization results for child agents. (a) Estimated trajectories of child agent 0 (blue) and child agent 1 (green). (b) Estimated x y positions of child agent 0. (c) Estimated x y positions of child agent 1.

Fig. 15. The error of the calculated distance between child agent 0 and 1. The distances are calculated using the estimated localization results. The average inter-agent range error is 0.064 m.

REFERENCES

[1] R. R. Pitre, X. R. Li, and R. Delbalzo, “UAV route planning for joint search and track missionsan information-value approach,” IEEE Trans. Aerosp. Electron. Syst., vol. 48, no. 3, pp. 2551–2565, 2012.
[2] P. Addabbo, A. Angrisano, L. M. Bernardi, G. Gagliarde, A. Mennella, M. Nisi, and S. L. Ulio, “UAV system for photovoltaic plant inspection,” IEEE Trans. Aerosp. Electron. Syst., vol. 53, no. 8, pp. 58–67, 2017.
[3] M. Maimone, Y. Cheng, and L. Matthies, “Two years of visual odometry on the mars exploration rovers,” J. Field Rob., vol. 24, no. 3, pp. 169–186, 2007.
[4] R. Dai, J. Maximoff, and M. Mesbahi, “Optimal trajectory generation for establishing connectivity in proximity networks,” IEEE Trans. Aerosp. Electron. Syst., vol. 49, no. 3, pp. 1968–1981, 2013.
[5] G. Vásárhelyi, C. Virág, G. Somorjai, T. Nepusz, A. E. Eiben, and T. Vicsek, “Optimized flocking of autonomous drones in confined environments,” Sci. Rob., vol. 3, no. 20, p. eaat3536, 2018.
[6] A. Kushleyev, D. Mellinger, C. Powers, and V. Kumar, “Towards a swarm of agile micro quadrotors,” Auton. Rob., vol. 35, no. 4, pp. 287–300, 2013.
[7] M. Hamer and R. DAndrea, “Self-calibrating ultra-wideband network supporting multi-robot localization,” IEEE Access, vol. 6, pp. 22 292–22 304, 2018.
[8] P. Müller, J. A. del Peral-Rosado, R. Piche, and G. Seco-Granados, “Statistical trilateration with skew-t distributed errors in LTE networks,” IEEE Trans. Wireless Commun., vol. 15, no. 10, pp. 7114–7127, 2016.
[9] J. Khalife and Z. M. Kassas, “Navigation with cellular CDMA signals part II: Performance analysis and experimental results,” IEEE Trans. Signal Process., vol. 66, no. 8, pp. 2204–2218, 2018.
[10] K. Shamaei, J. Khalife, and Z. M. Kassas, “Exploiting LTE signals for navigation: Theory to implementation,” IEEE Trans. Wireless Commun., vol. 17, no. 4, pp. 2173–2189, 2018.
[11] C. Yang, T. Nguyen, and E. Blasch, “Mobile positioning via fusion of mixed signals of opportunity,” IEEE Trans. Aerosp. Electron. Syst., vol. 29, no. 4, pp. 34–46, 2014.
[12] K. M. Pesyna, Z. M. Kassas, and T. E. Humphreys, “Constructing a continuous phase time history from TDMA signals for opportunistic navigation,” in Proc. ION/IEEE PLANS. IEEE, 2012, pp. 1209–1220.
[13] C. Yang and A. Soloviev, “Covariance analysis of spatial and temporal effects of collaborative navigation,” in Proc. ION/IEEE PLANS. IEEE, 2014, pp. 989–998.
[14] Y.-C. Wu, Q. Chaudhari, and E. Serpedin, “Clock synchronization of wireless sensor networks,” IEEE Signal Process. Mag., vol. 28, no. 1, pp. 124–138, 2011.
[15] B. Denis, J.-B. Pierrot, and C. Abou-Rjeily, “Joint distributed synchronization and positioning in UWB ad hoc networks using TOA,” IEEE Trans. Microw. Theory Tech., vol. 54, no. 4, pp. 1896–1911, 2006.
[16] R. M. Vaghefi and R. M. Buehrer, “Cooperative joint synchronization and localization in wireless sensor networks,” IEEE Trans. Signal Process., vol. 63, no. 14, pp. 3615–3627, 2015.
[17] B. Etlinger, F. Meyer, F. Hlawatsch, A. Springer, and H. Wyneersch, “Cooperative simultaneous localization and synchronization in mobile agent networks,” IEEE Trans. Signal Process., vol. 65, no. 14, pp. 3587–3602, 2017.
[18] L. Merino, J. Wiklund, F. Caballero, A. Moe, J. R. M. De Dios, P.-E. Forssen, K. Nordberg, and A. Ollero, “Vision-based multi-UAV position estimation,” IEEE Robot. Autom. Mag., vol. 13, no. 3, pp. 53–62, 2006.
[19] J. Ko, B. Stewart, D. Fox, K. Konolige, and B. Limketkai, “A practical, decision-theoretic approach to multi-robot mapping and exploration,” in Proc. IEEE/JSJ Int. Conf. Intell. Robots Syst., vol. 4. IEEE, 2005, pp. 3232–3238.
[20] D. Zou and P. Tan, “Coslam: Collaborative visual SLAM in dynamic environments,” IEEE Trans. Pattern Anal. Mach. Intell., vol. 35, no. 2, pp. 354–366, 2013.
[21] A. Howard, “Multi-robot simultaneous localization and mapping using particle filters,” Int. J. Rob. Res., vol. 25, no. 12, pp. 1243–1256, 2006.
[22] M. Basiri, F. Schill, D. Floreano, and P. U. Lima, “Audio-based localization for swarms of micro air vehicles,” in Proc. IEEE Int. Conf. Robot. Automat. IEEE, 2014, pp. 4720–4734.
[23] G. Sinibaldi and L. Marino, “Experimental analysis on the noise of propellers for small UAV,” Appl. Acoust., vol. 74, no. 1, pp. 79–88, 2013.
[24] J. Pugh, X. Raemy, C. Favre, R. Falconi, and A. Martinoli, “A fast onboard relative positioning module for multirobot systems,” IEEE/ASME Trans. Mechatronics, vol. 14, no. 2, pp. 151–162, 2009.
[25] T. Krajnık, M. Nitsche, J. Faigl, P. Vanˇek, M. Saska, L. Pˇreuˇcil, T. Duckett, and M. Mejail, “A practical multirobot localization system,” J. Intell. Robot. Syst., vol. 76, no. 3–4, pp. 539–562, 2014.
[26] I. Shames, B. Fidan, B. D. Anderson, and H. Hnam, “Cooperative self-localization of mobile agents,” IEEE Trans. Aerosp. Electron. Syst., vol. 47, no. 3, pp. 1926–1947, 2011.
[27] M. Z. Win and R. A. Scholtz, “Ultra-wide bandwidth time-hopping spread-spectrum impulse radio for wireless multiple-access communications,” IEEE Trans. Commun., vol. 48, no. 4, pp. 679–689, 2000.
[28] J.-Y. Lee and R. A. Scholtz, “Ranging in a dense multipath environment using an UWB radio link,” IEEE J. Sel. Areas Commun., vol. 20, no. 9, pp. 1677–1683, 2002.
[29] A. A. Ahmed, H. Shi, and Y. Shang, “Sharp: A new approach to relative localization in wireless sensor networks,” in Proc. Int. Conf. Distrib. Comput. Syst. Workshops. IEEE, 2005, pp. 892–898.
[30] N. Patwari, J. N. Ash, S. Kyperountas, A. O. Hero, R. L. Moses, and N. S. Correal, “Locating the nodes: cooperative localization in wireless sensor networks,” IEEE Signal Process. Mag., vol. 22, no. 4, pp. 54–69, 2005.
[31] R. M. Buehrer, H. Wymeersch, and R. M. Vaghefi, “Collaborative sensor network localization: Algorithms and practical issues,” Proc. IEEE, vol. 106, no. 6, pp. 1089–1114, 2018.

[32] D. L. Mills, “Internet time synchronization: the network time protocol,” IEEE Trans. Commun., vol. 39, no. 10, pp. 1482–1493, 1991.

[33] K. Römer, “Time synchronization in ad hoc networks,” in Proc. 2nd ACM Int. Symp. Mobile Ad Hoc Netw. Comput. ACM, 2001, pp. 173–182.

[34] J. Elson, L. Girod, and D. Estrin, “Fine-grained network time synchronization using reference broadcasts,” ACM SIGOPS Oper. Syst. Rev., vol. 36, no. SI, pp. 147–163, 2002.

[35] K.-l. Noh, E. Serpedin, and K. Qaraqe, “A new approach for time synchronization in wireless sensor networks: Pairwise broadcast synchronization,” IEEE Trans. Wireless Commun., vol. 7, no. 9, pp. 3318–3322, 2008.

[36] J. Zheng and Y.-C. Wu, “Joint time synchronization and localization of an unknown node in wireless sensor networks,” IEEE Trans. Signal Process., vol. 58, no. 3, pp. 1309–1320, 2010.

[37] S. Zhu and Z. Ding, “Joint synchronization and localization using toas: A linearization based WLS solution,” IEEE J. Sel. Areas Commun., vol. 28, no. 7, pp. 1017–1025, 2010.

[38] Y. Wang, J. Huang, L. Yang, and Y. Xue, “TOA-based joint synchronization and source localization with random errors in sensor positions and sensor clock biases,” Ad Hoc Netw., vol. 27, pp. 99–111, 2015.

[39] J. Morales and Z. M. Kassas, “Information fusion strategies for collaborative radio SLAM,” in Proc. ION/IEEE PLANS. IEEE, 2018, pp. 1445–1454.

[40] S. Bancroft, “An algebraic solution of the GPS equations,” IEEE Trans. Aerosp. Electron. Syst., no. 1, pp. 56–59, 1985.

[41] J. A. Barnes, A. R. Chi, L. S. Cutler, D. J. Healey, D. B. Leeson, T. E. McGunigal, J. A. Mullen, W. L. Smith, R. L. Sydnor, R. F. Vessot et al., “Characterization of frequency stability,” IEEE Trans. Instrum. Meas., no. 2, pp. 105–120, 1971.

[42] S. B. Moon, P. Skelly, and D. Towsley, “Estimation and removal of clock skew from network delay measurements,” in Proc. 18th Ann. Joint Conf. IEEE Comput. Commun., vol. 1. IEEE, 1999, pp. 227–234.

[43] Z. M. Kassas and T. E. Humphreys, “Receding horizon trajectory optimization in opportunistic navigation environments,” IEEE Trans. Aerosp. Electron. Syst., vol. 51, no. 2, pp. 866–877, 2015.

[44] T. Wang, “Cramer-rao bound for localization with a priori knowledge on biased range measurements,” IEEE Trans. Aerosp. Electron. Syst., vol. 48, no. 1, pp. 468–476, 2012.

[45] D. Neirynck, E. Luk, and M. McLaughlin, “An alternative double-sided two-way ranging method,” in Proc. IEEE 13th Workshop Positioning Navig. and Commun. IEEE, 2016, pp. 1–4.

[46] E. Karapistoli, F.-N. Pavlidou, I. Gragopoulos, and I. Tsetsinas, “An overview of the IEEE 802.15.4a standard,” IEEE Commun. Mag., vol. 48, no. 1, pp. 47–53, 2010.

[47] Y. Jiang and V. C. Leung, “An asymmetric double sided two-way ranging for crystal offset,” in Proc. Int. Symp. Signals, Syst. Electron. IEEE, 2007, pp. 525–528.

[48] R. G. Brown and P. Y. Hwang, Introduction to random signals and applied Kalman filtering. Wiley New York, 1992.