**Performance of Sagnac Interferometer with Loops Made of PCF and PANDA Fibers**

**Abstract**

The parametric effects on performance of the Sagnac interferometer with loop (SLI) made of high-birefringence photonic crystal fiber (HB-PCF) and polarization-maintaining and absorption reducing (PANDA) fibers are simulated and analyzed accordingly in this paper where transmission spectra and the variations of free spectral range are studied under different conditions. The obtained results from calculations and comparisons of the curves loop fiber made of standard polarization-maintaining fiber and high-birefringence photonic crystal fibers revealed that the distance between fringes (DBF) of the SLI would reduce by increasing loop length. This reducing trend in case of HB-PCF has steeper slope. The DBF for two fibers HB-PCF and PANDA with shorter loop lengths would increase.

This study reveals that by using high-birefringence PCF, one can optimize the loop length with minimum distance between fringes in the Sagnac loop interferometer. The obtained results provide a required condition for fabrication of SLI-based devices, such as optical sensors, with a small packaging size.

**Keywords:** Sagnac Interferometer; Loop length; HB-PCF; PANDA fiber; Free spectral range; Performance

**Abbreviations:** HB-PCF: High-Birefringence Photonic Crystal Fiber; DBF: Distance Between Fringes; SLI: Sagnac Loop As a Interferometer; WDM: Wavelength Division Multiplexing; PCFs Photonic Crystal Fibers; FSR: Free Spectral Range

**Introduction**

Optical fiber Sagnac loop as a interferometer (SLI), is a useful component utilized in devices and systems of optical technology [1-2]. As of today, several components based on SLI, have been designed for applications of wavelength division multiplexing (WDM) filters and optical sensors, using conventional and photonic crystal fibers [3-6]. In an SLI, two interfering waves in an optical fiber loop counter-propagate in a similar path. Usually, a standard optical fiber Sagnac loop made of a birefringent fiber in a comparison to Mach-Zehnder interferometer has several advantages, such as insensitivity to temperature, high extinction ratio, and independent to input polarization of light waves [7].

Amongst various features of photonic crystal fibers (PCFs), one of the characteristics is their capability of producing high birefringence by merely changing the core and rearranging the geometry of the air-holes placed along the dadding region. It is possible to obtain a birefringence as high as $10^{-5}$, which is twice the value in standard single-mode fibers [8]. In polarization-maintaining fibers, such as Polarization-maintaining and absorption reducing PANDA fibers, elliptical core fiber, and bow-tie fibers, that have at least two regions of different material with different thermal expansion coefficients in the core region, the polarization of propagating wave changes when the environmental temperature varies with time [9]. On the contrary, the birefringence of PCFs is insensitive to thermal changes, because it is made of a single material.

In this paper, the parametric effects on performance of the Sagnac interferometer with loop made of high-birefringence PCF (HB-PCF) and PANDA fibers are simulated and analyzed accordingly, where transmission spectra and the variations of free spectral range (FSR) are studied under different conditions.

**SLI with PCF loop**

A schematic diagram of a SLI is shown in Figure 1 in which the loop is made of an HB-PCF [10] or PANDA fiber by connecting two output ports of a directional coupler with a coupling coefficient of $K = 0.5$ [11]. The input light to arm 1 of the 3-dB directional coupler is divided into two equal intensity counter-propagating waves, entering the loop from port 3 and 4. The coupled light to the loop faces a phase delay of $\pi/2$, thus the intensity of the transmitted light to the arm 2 will equal to the summation of two fields with equal amplitudes, one in clockwise with an optional phase of $\phi$ and the other field in anti-clockwise with a relative phase of $\phi - \pi$. As a consequence, the transmitted field intensity will become zero and the input light maintaining all the energy will reflect back to arm 2.

The presence of birefringence in the fiber causes a velocity difference and optical path variation related to state of polarization. As a result, when these fields once again enter the directional coupler, will retain a relative phase difference. Therefore, the reflection will become zero and the fields in the coupler recombine, and the resulting light appears at the interferometer output. The interference of the propagated fields in the loop, depending on the birefringence, may either be constructive or destructive.
Irrespective of coupler loss and field evanescence of birefringent fiber of the loop, the transmission $T$ coefficient and reflection coefficient $R$ of the loop are nearly periodic functions expressed as:

$$T = \frac{1 - \cos(\delta)}{2} \quad (1)$$

$$R = \frac{1 + \cos(\delta)}{2} \quad (2)$$

where $\delta = \left( \frac{2\pi\Delta n_g L}{\lambda} \right)$ denotes the phase difference between polarization modes of high-birefringence where $\Delta n_g$ is the fiber group birefringence, $L$ is the loop length, and $\lambda$ represents the wavelength of the light in vacuum.

When the variations of $\Delta n_g$ are small in comparison to the wavelength, then $\Delta n_g \approx n_x - n_y$, where $n_x$ and $n_y$ are the effective refractive indices of polarization modes in $x$ and $y$ direction, respectively. The maximum wavelengths act as resonance wavelengths that are represented as:

$$\lambda = \frac{2\pi\Delta n_g L}{(2m+1)\pi} \quad (3)$$

where $m$ is an integer. The wavelength difference between two adjacent maxima (fringe distance) is determined by the relation

$$\Delta \lambda = \lambda^2 / (\Delta n_g L) \quad (5)$$

**Simulation of Transmission Spectrum of the SLI**

With reference to Eq. 3, the distance between fringes (DBF), i.e., $\Delta \lambda$, in SLI is inversely proportional to the loop length. Thus, to obtain the smallest distance between fringes, we need longer loop length made of HB-PCF.

For a comparison, the DBF as a function of loop length of two types of loop fiber, one an HB-PCF with a high group birefringence of $\Delta n_g = 8.56 \times 10^{-4}$ and the other a PANDA fiber with group birefringence of $\Delta n_g = 3.3 \times 10^{-4}$ both at wavelength $\lambda = 1550\text{nm}$, is depicted in Figure 2.

By comparing the variations of the DBF in terms of loop lengths for the PANDA and the HB-PCF fibers, it is found that the DBF for the two fibers is more for shorter loop lengths. It’s further revealed that in HB-PCF, by decreasing the loop length, the trend of increase of the DBF is with smaller slope as compared to the case of PANDA fiber. Further, by reduction of the loop length, the DBF faces more variation when the PANDA fiber is used as the loop.

To study the transmission spectrum and the analysis of spectral response with respect to loop length variations, the simulations are performed by using the solver software MATLAB, as depicted in Figure 3. In Figure 3a, the loop length is taken as 50 cm, whereas in Figure 3b, the loop is 20 cm long.

On comparing these curves, we note that when loop length becomes shorter, the DBF in SLIs with two types of fiber used in the loop would considerably increase. By assessing Figures 3a & 3b, we can extract a relationship between free spectral range (FSR) and group refractive index related to two types of fibers, HB-PCF and PANDA, as follows:

$$\Delta \lambda_{\text{PANDA}} \approx 2.5 \Delta \lambda_{\text{HB-PCF}} \quad (4)$$

$$\Delta n_g(\text{HB-PCF}) \approx 2.5 \Delta n_g(\text{PANDA}) \quad (5)$$

Therefore, by multiplying above expressions, we get:

$$(\Delta \lambda_{\text{PANDA}} \Delta n_g)_{\text{PANDA}} \approx (\Delta \lambda \Delta n_g)_{\text{HB-PCF}} \quad (6)$$

If the transmission spectrum of the SLI is illustrated for each fiber for different loop lengths, as shown in Figures 4a & 4b, the derived relationship between $\Delta \lambda$ and $\Delta n_g$ will be similar to the previous expression that is not dependent on the loop length.

**Variations of FSR in terms of Group Birefringence**

By using PCF with higher group birefringence, the FSR will reduce. To study the trend of variations, the two expressions considered for two PCFs with birefringence of $\Delta n_g = 8.65 \times 10^{-4}$ and $\Delta n_g = 27.67 \times 10^{-4}$, are simulated and then illustrated in Figure 5.
The transmission spectrum of the SLI with a loop length of 20 cm made of the PCF with birefringence of $\Delta n_g = 27.67 \times 10^{-4}$ is depicted in Figure 6. On a comparison, one can observe that the DBF of the SLI with a loop length of 20 cm made of HB-PCF in Fig. 6 is approximately one third of the DBF in Figure 4a.

**Figure 3:** Transmission spectrum of the SLI for HB-PCF loop and PANDA loop with equal loop length of 20 cm.

**Figure 4:** Transmission spectrum of the SLI (a) for HB-PCF and (b) PANDA fiber with different loop lengths.

**Figure 5:** Free spectral range versus loop length made of two PCFs with birefringence (a) $\Delta n_g = 8.65 \times 10^{-3}$ and (b) $\Delta n_g = 27.67 \times 10^{-4}$.

**Figure 6:** The transmission spectrum of the SLI with loop fiber HB-PCF of $L = 20$ cm and $\Delta n_g = 27.67 \times 10^{-4}$.
Discussion

The DBF for the loop length of 20 cm made of PANDA fiber is 36.4 nm, while for the HB-PCF used as the loop fiber, the DBF is obtained as 13.88 nm. The difference of the DBF between two cases is 22.5 nm, or in other words, when miniaturization of SLI is required with short loop lengths, employment of HB-PCF is preferred where the value of DBF would reduce more than half of the value.

The comparison between two HB-PCF fibers, one with \( \Delta n_g = 8.65 \times 10^{-4} \) and the other with \( \Delta n_g = 27.67 \times 10^{-4} \) is carried out and the obtained results show that the reducing slope of the curve for HB-PCF loop with group birefringence of more than \( \Delta n_g = 27.67 \times 10^{-4} \) is more and the DBF is less than that of HB-PCF with \( \Delta n_g = 8.65 \times 10^{-4} \).

Yet, in another study, the transmission spectrum of the SLI in terms of wavelength for two fiber samples with loop lengths of 20 cm and 50 cm is simulated. The comparison of the distance between maxima in the obtained characteristic curves, certifies the calculated DBF values versus loop length.

Conclusion

In the present paper, the relationship between the wavelength of consecutive maxima in transmission spectrum in terms of loop length of Sagnac loop interferometer is established and analyzed with loop fibers made of HB-PCF and PANDA fiber. The obtained results from calculations and comparisons of the curves loop fiber made of standard polarization-maintaining fiber and high-birefringence photonic crystal fibers revealed that the distance between fringes (DBF) of the SLI would reduce by increasing loop length. This reducing trend in case of HB-PCF has a steeper slope. The DBF for two fibers HB-PCF and PANDA with shorter loop lengths would increase. As an example, the DBF with the loop length of 150 cm made of PANDA fiber is \( \Delta \lambda = 14.57 \) nm, whereas for HB-PCF with equal loop length with \( \Delta n_g = 8.65 \times 10^{-4} \), the DBF is obtained as \( \Delta \lambda = 5.55 \) nm. That is, the DBF of SLI with loop length of 50 cm made of HB-PCF, is 9 nm smaller than the SLI with the loop made of PANDA fiber.

By the obtained results through simulations, this study reveals that by using high-birefringence PCF, one can optimize the loop length with minimum distance between fringes in Sagnac loop interferometer. The obtained results provide a required condition for fabrication of SLI-based devices with a small packaging size.

Acknowledgement

The authors would like to acknowledge the optical communication group management for permission of publication of the present paper.

Conflict of Interest

None.

References

1. Fu HY, Tam HY, Shao LY (2008) Pressure sensor realized with polarization-maintaining photonic crystal fiber-based Sagnac interferometer. Appl Opt 47(15): 2835-2839.
2. Kim G, Cho T, Hwang K (2009) Strain and temperature sensitivities of an elliptical hollow-core photonic bandgap fiber based on Sagnac interferometer. Opt Exp 17(4): 2481-2486.
3. Mortimore DB (1988) Fiber loop reflectors. J Lightwave Technol 6(7): 1217-1224.
4. Yang S, Li Z, Dong X, Kai G, Zhao Q (2002) Generation of wavelength-switched optical pulse from a fiber ring laser with an F-P semiconductor modulator and a HiBi fiber loop mirror. IEEE Photon Technol. Lett 14: 774-776.
5. Hae Young Choi, Myoung Jin Kim, Byeong Ha Lee (2007) All-fiber Mach-Zehnder type interferometers formed in photonic crystal fiber. Opt Exp 15(9): 5711-5720.
6. Xiaojun Fang, Richard O Claus (1995) Polarization-independent all-fiber wavelength-division multiplexer based on a Sagnac interferometer. Opt Lett 20(20): 2146-2148.
7. Kim DH, Kang IU (2004) Sagnac loop interferometer based on polarization maintaining photonic crystal fiber with reduced temperature sensitivity. Opt Exp 12(19): 4490-4495.
8. Hansen TP, Broeng J, Libori SEB, Knudsen E, Bjarklev A, et al. (2001) Highly birefringent index-guiding photonic crystal fibers. IEEE Photon Technol Lett 13(6): 588-590.
9. Chun-Liu Zhao, Xinfeng Yang, Chao Lu, Wei Jin, Demokan MS (2004) Temperature-Insensitive Interferometer Using a Highly Birefringent Photonic Crystal Fiber Loop Mirror. IEEE Photon Technol Lett 16(11): 2535-2537.
10. Ortigosa-Blanch A, Knight JC, Wadsworth WJ, Arriaga J, Mangan BJ, et al. (2000) Highly birefringent photonic crystal fibers. IEEE Photon Technol Lett 12(16): 2357-2359.
11. Wang YI, Zhao CL, Dong X, Kang J, Jin S (2011) A fiber loop mirror temperature sensor demodulation technique using a long-period grating in a photonic crystal fiber and a band-pass filter. Rev Scientific Instru 82(7): 073101.