Introduction

Fractal analysis is a very useful tool in the understanding of many phenomena in various fields, such as astrophysics, economics, biology and medicine. Interesting results have also been achieved in bacteriology, medical imaging and ophthalmology (e.g. diabetic retinopathy) [1-6].

Retinal vascular network in healthy subjects has a value of fractal dimension [7], close to the value of a Diffusion-Limited Aggregation (DLA) process \( D=1.70 \) [8], while in pathologic condition that value changes deeply. We can recall papers by Cavallari et al. [9], that showed a reduction in complexity of retinal vessels, reflecting the alteration of the brain microvessels in patients with cerebral autosomal dominant arteriopathy with subcortical infarcts and leukoencephalopathy (CADASIL) and the ones by Doubal et al. [10], that found a low value of retinal vessels fractal dimension associated to the lacunar stroke and by Ţalu et al. that, recently, showed that fractal analysis is able to characterize the human non-proliferative diabetic retinopathy [11]. In these works, fractal analysis has been demonstrated a sensitive tool to assess changes of retinal vessel branching, able to reflect the early microvessel alterations in human pathology. Moreover, the retina vessels network, described by generalized dimensions and singularity spectrum, has a multifractal structure (an object having different fractal properties in its different region) [12]. These multifractal approaches were able to characterize the retinal vascular architecture disorder in several diseases [11,13,14].

At initial presentation, the differential diagnosis between optic neuritis (ON) and nonarteritic anterior ischemic optic neuropathy (NAION) is difficult to be performed on clinical grounds, both giving overlapping clinical profiles [15]. However, it is fundamental to establish an early differential diagnosis, having the ON patient a clear tendency to develop multiple sclerosis, a disease where therapies should be performed as early as possible [16]. In order to verify whether the fractal analysis of the optic nerve head microvasculature could help in the differential diagnosis between ON and NAION, we have evaluated the mass dimension of the optic nerve head vascular pattern, as revealed by fluorescein angiography.

Subjects

Patients with unilateral NAION or unilateral idiopathic ON were recruited from the Department of Ophthalmology of the University of Siena. Each patient underwent a complete neuro-ophthalmic examination, including assessment of visual acuity, colour vision, papillary reaction, slit-lamp examination, applanation tonometry, Goldman visual field testing, visual evoked potentials, dilated fundoscopy and fluorescein angiogram.

The criteria for patients’ admittance with NAION to the study were: unilateral disc swelling with clinical features consistent with NAION [16], no recovery of visual function in the first month of follow up, exclusion of arteritic anterior ischemic optic neuropathy either on clinical grounds or following a negative temporal artery biopsy, negative magnetic resonance imaging of the brain and orbits, no other ocular pathology, no neurological diseases that might influence or explain the patient’s visual symptoms. The patient admittance criteria with ON for the present research were: unilateral visual impairment associated with impaired colour vision and visual-field loss, presence of Siena. Each patient underwent a complete neuro-ophthalmic examination, including assessment of visual acuity, colour vision, papillary reaction, slit-lamp examination, applanation tonometry, Goldman visual field testing, visual evoked potentials, dilated fundoscopy and fluorescein angiogram.

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of disc oedema, young age (≤ 35 years), ocular pain associated with eye movements, recovery of visual function in the first month of follow up, no other ocular pathology, no neurological diseases that might influence or explain the patient’s visual symptoms; history or detection of multiple sclerosis confirmed the diagnosis [17].

Nine cases of NAION and nine cases of ON with presence of optic disc oedema were enrolled without any selection. The unaffected eye of the patient was used as control (n=10). All patients were examined using a fluorescein angiogram within the first two weeks after they reported the first symptoms and before treatments; all patients gave informed consent. The protocol for this research project was approved by the Ethics Committee of the University of Siena and it conforms to the provisions of the Declaration of Helsinki, 1955 (as revised, Edinburgh, 2000).

Image analysis

Static fluorescein angiogram was performed (IMAGEEnet 2000.v.2.0, Topcon). The early, intermediate and late phases of the angiogram were studied. Images of the early venous phase of the angiogram (around 20 seconds) gave the best visualization of the optic disc vessels and were saved. The same magnification was used for every patient.

A manual outline of the trajectories of the two-dimensional microvascular network was performed down to microvessels of 20 micron of diameter, processed to threshold the vessel network without background interference and converted into an outline of one pixel by means of Jmicrovision, http://www.jmicrovision.com, and Image Analyzer, http://www.fosshub.com/Image-Analyzer.html, softwares.

Mass Dimension (Dm)

The images were represented on a graphic window of 500 x 500 pixels (1 pixel = 4 μm). To evaluate the mass dimension of the pattern, the set was covered with circles of radius r, (from 20 to 200 pixels), and the amount of pixels (n) inside the circles was evaluated [7]. A log-log plot was performed. The plot of the logarithm of n against the logarithm of r produced a straight line with a slope equal to Dm.

The methodology was implemented using Benoit 1.3 software (TruSoft Int’l Inc, http://trusoft-international.com/.html) and validated measuring computer generated Euclidean and fractal shapes of known mass dimensions. Inter- and intra-observers errors were < 3%.

Statistical analysis

Mann-Whitney’s U test was used in order to compare the mass dimension indexes and to ascertain the significance among the groups; regression analysis was used to ascertain the log-log plot linearity. Receiver Operator Characteristic (ROC) were obtained with XLSTAT software (www.xlstat.com). Variance analysis was used in order to ascertain the dependence of the fractal index by age or gender.

Results

Images of the early venous phase of the angiogram (around 20 seconds) gave the best visualization of the optic disc vessels (Figure 1).

Image processing was able to reveal the microvascular pattern of the optic nerve head (Figure 2).

Fractal analysis showed that the optic nerve head microvasculature is fractal (log-log plot, r > 0.99, Figure 3).

Mass dimension statistically distinguished three classes (health condition vs. NAION vs. ON patients with optic disc oedema (Table 1).

| Subjects                        | Dm (SD)        |
|--------------------------------|---------------|
| ON* with optic disc oedema     | 1.94 (0.025) * * |
| NAION†                         | 1.86 (0.03) * |
| Control                        | 1.74 (0.03)   |

*optic neuritis
†nonarteritic anterior ischemic optic neuropathy.

ROC curves showed high sensitivity and specificity of the measures in order to distinguish among controls and pathologies (Figures 4,5).

Age and gender of patients doesn’t affect the results (p>0.05; p>0.05).

Discussion

Recovery of visual function, visual field testing abnormalities, pain induced by ocular movements, cup-to-disc ratio, presence and/or distribution of optic disc oedema and fluorescein angiography together which age at diagnosis may help to differentiate optic neuritis (ON) and nonarteritic anterior ischemic optic neuropathy.
**Figure 2**: Trajectories of the optic nerve head microvasculature after fluorescein angiogram and image analysis. Control eye (left); nonarteritic anterior ischemic optic neuropathy (NAION, middle); optic neuritis with optic disc oedema (ON, right).

**Figure 3**: Log log plots. Plots present a straight line: the pattern is fractal. The exponent is the mass dimension of the optic nerve head microvasculature after fluorescein angiogram. Control eye (left), optic neuritis (right).

**Figure 4**: ROC curve. Health condition vs. non-glaucomatous disorders. Sensitivity = 0.98, Specificity = 0.96, p < 0.0001.
To facilitate early diagnosis, researchers have focused on objective morphological analysis of the retrobulbar tract and the head of the optic nerve, in order to reduce the bias caused by subjective medical interpretations [20]. Optic nerve analysis by means of magnetic resonance imaging, digital stereoscopy and Heidelberg retina tomography are some examples of how recent technologies can quantitatively document peculiar clinical findings in ON, NAION and other optic nerve diseases [21-23]. We can also recall the laser-based blood flow measuring technique applied to the study of optic nerve head microcirculation that has been able to quantitatively demonstrate optic nerve head circulatory abnormalities in patients with ON and NAION [24]. However, even by using these different approaches, ON and NAION frequently present overlapping clinical profiles, and sometimes appears difficult to distinguish them on clinical grounds at initial presentation [15].

In the present study, we have studied by means of fractal analysis the vascular patterns of optic nerve head obtained using fluorescein angiography in patients affected by ON and NAION. We then correlated the mass dimension values with the clinical diagnosis.

The validity of this method is confirmed by the concordance between the mass dimension values of the optic nerve head in the control group obtained by us and the fractal indexes obtained in normal retinal vessel by other Authors [25-29]. These values correspond to the complexity value of a diffusion limited aggregation (DLA) model [30], characteristic of many physiological structures [31-33].

The evaluation of mass dimension values in NAION and in ON patients showed significantly higher values compared with controls. In particular, the mass dimension in the ON group with optic disc oedema showed the highest value, corresponding to the highest complexity of the vascular pattern of the optic nerve head and represented by almost complete filling of the plane.

Mass dimension values in the NAION were approaching the one of a percolation model [34,35], in NAION a 2nd order phase transition arises. The changing state means that the vessel growth does not follow according to nonlocal gradient value of diffusible growth factors, a diffusion-limited growth process as in our normal vascular retina, but according to a mechanism related to variables that act locally, variables like stress, local concentration of angiogenic molecules, or, more likely, irregular, inhomogeneous, substrate, as observed in the tumor vascular architecture [36].

Mass dimension values in the ON group with optic disc oedema showed the highest mean fractal dimension value: the distribution of the vascular pattern of the optic nerve head is completely chaotic, almost completely filling the plane. A clear effect of the tissue flogosis, even if this last result might be biased by the presence of the disc oedema, able to alter the local geometry of the blood vessels and generating a difficult visualization of the geometric pattern itself.

In the present paper, mass dimension of the optic nerve microvascularity observed by fluorescein angigram appears able to objectively quantify the optic nerve head microvasculature and to distinguish among ON, NAION and health condition with high sensitivity and specificity, giving us a new tool in order to help clinicians to perform early diagnosis and to follow therapeutic procedures. These results add also new information to previous data obtained by us, where another fractal index, geometrical complexity evaluated by local box-counting analysis, resulted able to distinguish between the pathologies [37].

The new fast and unexpensive methodology here described appears clearly able to help clinicians to perform differential diagnosis between non-glaucomatous optic neuropathies, it might be useful also in order to study the effect of therapies during the follow up of the patient.

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