Observation of the Same New Sheet Topology in Both the Layered Uranyl Oxide-Phosphate \( \text{Cs}_{11}\[(\text{UO}_2)_{12}(\text{PO}_4)_3\text{O}_{13}] \) and the Layered Uranyl Oxyfluoride-Phosphate \( \text{Rb}_{11}\[(\text{UO}_2)_{12}(\text{PO}_4)_3\text{O}_{12}\text{F}_2] \) Prepared by Flux Crystal Growth

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Single crystals of four new layered uranyl phosphates, including three oxyfluoride-phosphates, were synthesized by molten flux methods using alkali chloride melts, and their structures were determined by single-crystal X-ray diffraction. \( \text{Cs}_{11}\[(\text{UO}_2)_{12}(\text{PO}_4)_3\text{O}_{13}] \) (1) and \( \text{Rb}_{11}\[(\text{UO}_2)_{12}(\text{PO}_4)_3\text{O}_{12}\text{F}_2] \) (2) contain uranyl phosphate layers exhibiting a new sheet topology that can be related to that of \( \beta\text{-U}_3\text{O}_8 \), while \( \text{Cs}_{4.4}\text{K}_{0.6}\[(\text{UO}_2)_{6}\text{O}_4\text{F}(\text{PO}_4)_4(\text{UO}_2)] \) (3) and \( \text{Rb}_{4.4}\text{K}_{0.6}\[(\text{UO}_2)_{6}\text{O}_4\text{F}(\text{PO}_4)_4(\text{UO}_2)] \) (4) contain layers of a known isomer of the prominent phosphuranylite topology. The location of the fluorine in structures 2-4 is discussed using bond valence sums. First principles calculations were used to explore why a pure oxide structure is obtained for the Cs containing phase (1) and in contrast an oxyfluoride phase for the Rb containing phase (2). Ion exchange experiments were performed on 1 and 2 and demonstrate the ability of these structures to exchange approximately half of the parent alkali cation with a target alkali cation in an aqueous concentrated salt solution. Optical measurements were performed on 1 and 2 and the UV-vis and fluorescence spectra show features characteristic of the \( \text{UO}_2^{2+} \) uranyl group.

Keywords: flux crystal growth, uranyl, phosphuranylite, single crystal, DFT

INTRODUCTION

Nuclear power has been well-established for several decades and, nonetheless, studies continue to develop a deeper understanding of the nuclear fuel cycle, including exploring improved methods of both long-term and short-term waste storage (zur Loye et al., 2018), and continuing to investigate the processes of radionuclide leaching into surrounding ecosystems.
For these reasons, it is advantageous to further expand our understanding of uranium coordination chemistry, specifically in extended structures, as this can give us insights in understanding intermediate phases in the nuclear waste cycle, identifying potential structures useful in nuclear waste processing or storage, and possible pathways within the environment for the migration of U(VI) and other actinides.

Nature often gives a good indication of what chemical compounds can be made synthetically. For example, uranium containing minerals present a few prominent sheet anion topologies that can be observed both in minerals and synthetic compounds. In Lussier et al. (2016) most recent review of hexavalent uranium compounds, autunite, phosphuranylite, and uranophane are significant minerals classes with 40 proposed autunite minerals, 16 phosphuranylite, and 10 uranophane minerals. Phosphuranylite and autunite minerals are the primary classes of phosphorus containing minerals, as phosphorus bearing uranium minerals make up nearly a quarter of all identified uranium minerals. The uranophane topology is specifically prominent among silicates, but as in the phosphuranylite topology the tetrahedrally coordinated Si or P sites can be replaced by other tetrahedrally—or even trigonal pyramidal or trigonal planar—coordinating elements. These sheet anion-topologies common among minerals have also been observed in numerous synthetic compounds including 38 belonging to the autunite, 18 belonging to the uranophane, and 16 belonging to the phosphuranylite classes (Lussier et al., 2016; Wang et al., 2017; Juillerat et al., 2018a; Juillerat and zur Loye, 2019).

While nature certainly gives a good indication of what we might be able to synthesize in the laboratory, many additional sheet topologies outside of those found in minerals are also reported [62 reported in Lussier et al. (2016)]. All of the discussed sheet topologies so far have been for uranium oxide compounds and one way to expand the number of known sheet topologies, and thus our understanding of uranium chemistry, is to partially exchange oxygen within these sheets with other anions such as halides. While one may expect to make radically different sheet structures using Cl− due to the commonly terminal nature and large size of this anion, causing it to stick out of the plane of the sheet, as seen in K4U3O16Cl2 and Cs5U2O22Cl3 (Read et al., 2014), the inclusion of F− could lead to new sheet structures or to those already observed in oxides. This arises partially due to the similarity in size of O and F, and examples can be seen in the existence of both rare earth oxides and oxyfluorides that adopt the prominent apatite structure (Latshaw et al., 2014, 2015). In rare earth silicates, the coordination of the rare earth to F limits the available connectivity to the silicate tetrahedra, as SiO3F tetrahedra are unreported in crystalline structures (Leinenweber et al., 2005; Morrison et al., 2016). Although PO3F tetrahedra exist, i.e., Sr(PO3F), they have yet to be reported in uranium extended structures, although it is unclear whether this is due to chemical principles or whether the proper conditions for this structure motif have yet to be explored.

Herein we present the synthesis and structural characterization of two examples of uranium oxyfluorides that adopt the phosphuranylate topology, Cs4.4K0.6[(UO2)6O4F(PO4)4(UO2)] (3) and Rb4.4K0.6[(UO2)6O4F(PO4)4(UO2)] (4), and a new sheet anion topology that is observed for both a pure oxide, Cs11[(UO2)12(PO4)3O13] (1), and an oxyfluoride, Rb11[(UO2)12(PO4)3O11F2] (2).

EXPERIMENTAL

Synthesis

Compounds 1-4 were synthesized via molten flux methods using alkali chloride fluxes (Bugaris and zur Loye, 2012; Juillerat et al., 2019a). For all reactions UF4 (International Bio-Analytical Industries, powder, ACS grade) was used as the uranium starting material, AlPO4 (Alfa Aesar, powder, 99.99%) was used as the phosphorus source, and an alkali halide, CsCl (Alfa Aesar, powder, 99.99%), KCl (Mallinckrodt Chemicals, powder, 99.6%), or RbCl (Alfa Aesar, powder, 99.8%), or a mix thereof was used as a flux. Caution! Although the uranium precursor used contained depleted uranium, standard safety measures for handling radioactive substances must be followed. Generally, all solid reactants were loaded into either an alumina or platinum crucible and heated to 875°C in 1.5 h, held at this temperature for 12 h, then cooled at 6°C/h to 550 or 450°C depending on the melting point of the flux. After slow cooling, the furnace was shut off and allowed to rapidly cool to room temperature before sonicking the reaction mixtures in water to remove the flux and isolate the crystalline products by vacuum filtration.

Cs11[(UO2)12(PO4)3O13] (1) was synthesized by loading 1 mmol UF4, 0.25 mmol AlPO4, and 20 mmol of CsCl in a platinum crucible with a loose-fitting platinum lid and was slow cooled to 550°C. The reaction produced red tablets (Figure 1) in a nearly quantitative yield with no identifiable by-products. Rb11[(UO2)12(PO4)3O11F2] (2) was obtained by loading 0.5 mmol UF4, 0.125 mmol AlPO4, and 20 mmol of RbCl into a small alumina crucible in a concrete holder with a larger inverted crucible covering it. This mixture was heated as mentioned above and slow cooled to 550°C and produced similar looking orange-red tablets as in 1 in a nearly quantitative yield with no identifiable byproducts. Cs4.4K0.6[(UO2)6O4F(PO4)4(UO2)] (3) and Rb4.4K0.6[(UO2)6O4F(PO4)4(UO2)] (4) were obtained from reactions of 0.5 mmol UF4, 0.2 mmol AlPO4, and 5 mmol CsCl or RbCl and 5 mmol KCl loaded into an alumina crucible covered with an alumina plate held in place by rubber cement. These were heated and slow cooled to 450°C and produced a yellow crystalline product identified as a mixture of the newly reported F containing phases and either Cs4K4−x[(UO2)3(PO4)2] or Rb1.2K2.6[(UO2)3(PO4)3O2] that are visibly indistinguishable. The purity and identity of the products were determined by powder X-ray diffraction (PXRD) using a Bruker D2 Phaser equipped with a LYNXEYE silicon strip detector using a Cu Kα (λ = 1.54056 Å) source.

Structure

The reported structure solutions were obtained from single crystal X-ray diffraction (SXD) data collected on a Bruker D8 QUEST diffractometer equipped with an Incoatec IPDS 3.0.
microfocus radiation source (Mo Kα, λ = 0.71073 Å) and a PHOTON II area detector. The reduction absorption correction was applied to the raw data using SAINT+ and SADABS within the APEX3 software (Bruker, 2015). The SHELXL suite was used within the OLEX2 GUI to solve the structure using SHELXTL and refine the solution using SHELXL (Sheldrick, 2015a,b). The TWINROTMAP functionality in PLATON was used to check for missed symmetry elements and twin laws, where 

\[
\text{Table 1} 
\]

In all structures the refinement of the U sites is straightforward, while in all structures there is disorder among the alkali cation sites, and in structures 1 and 2 there is disorder in one of the phosphate tetrahedra. Generally, the disorder in the alkali sites was treated by freely refining the sites as Cs or Rb as appropriate, and if less than one, then it was assumed that either the sites is shared by a smaller alkali cation, K⁺ in 3 and 4, or a disordered site across multiple positions. The presence of significant nearby electron density peaks suggests a disordered site, while the absence of these suggests sharing of the site between Cs/K or Rb/K. Mixed sites, and multiple disordered sites were constrained to occupancies of one using free variables or SUMP commands in cases of more complicated disorder, and the use of ISOR and EADP commands were implemented to constrain thermal parameters. The full details of the structure refinements are located in Supporting Information and the checkoff report is contained in Supplementary Data Sheet 1.

In structures 1 and 2 the P3 site is half occupied because it is disordered across a mirror plane and the two disordered sites are too close to both be fully occupied sites. This is also true for O23, O27, O28 which are disordered in site 2 and O29 coordinated to P1 in 1, and O28A and F28B in 2. Labeling all sites within the coordination sphere of the U sites as O in structures 2-4, does not result in charge balance, as there is an excess of negative charge. This could not be resolved by reasonable models of the alkali cation disorder and this observation, along with the identification of F in all three structures by EDS in both powder and singly crystalline forms, confirms the presence of F. While the fluorine site could be easily located in structure 2 by using bond valence sums (BVS) and knowledge of U coordination chemistry (discussed in structure description), it was not easily identified in 3 and 4. In 3 and 4 the O3 site was fixed as a half occupied O/F shared site to maintain charge balance in the crystallographic solution, and this arbitrary assignment will be discussed in later sections.

EDS was used to verify the presence of F in 2-4 and all other elements present in each single crystal used for structure determination as well as in bulk powder samples of 1 and 2. Data were collected on a TESCAN Vega-3 SBU equipped with an EDS detector.

**Optical Spectroscopy**

UV-vis and fluorescence measurements were performed on bulk powder samples of 1 and 2 using a PerkinElmer Lambda 35 UV-vis scanning spectrophotometer equipped with an integrating sphere and a PerkinElmer LS55 Luminescence spectrometer. The UV-vis diffuse reflectance data were internally converted using the Kubelka-Munk equation and then normalized (Kubelka and Munk, 1931). Fluorescence excitation spectra were collected at emission wavelengths of 574 and 564 nm for 1 and 2, respectively, and emission spectra were collected at an excitation wavelength of 437 nm for both 1 and 2.

**Ion Exchange**

Ion exchange experiments were performed on powder and single crystalline samples of Cs11[2(PO4)2]UO212 (1) and Rb11[2(PO4)2]UO212F2 (2), where 20 mg of sample was soaked in ~4 mL of concentrated salt solution in a drying oven set to 90°C for 3 days. The Rb analog, 2, was soaked in 11 m CsCl solutions while the Cs analog, 1, was soaked in 7 m RbCl or 4 m KCl solutions. Products were examined by EDS and PXRD as described above.

**First Principles Calculations**

We used first-principles calculations using the density functional theory (DFT) code VASP (Vienna Ab-initio Simulation Package) (Kresse and Furthmuller, 1996a,b) employing the projector augmented wave (PAW) method (Blochl, 1994; Kresse and Joubert, 1999) and generalized gradient approximation of Perdew, Burke and Ernzerhof (PBE) (Perdew et al., 1996) to model the systems. These were spin-polarized calculations, using a plane wave basis set with an energy cut-off of 520 eV to expand the electronic wave functions, and 10⁻⁶ eV energy convergence criteria. A 2 × 2 × 2 k-point mesh was used for sampling the Brillouin zone. The ground state geometries at 0 K were obtained by relaxing the cell volume, atomic positions, and cell symmetry until the maximum forces on each atom were <0.01 eV/Å. To better represent the correlated nature of the U f-electrons, we employed the DFT+U method (Anisimov et al., 1993; Liechtenstein et al., 1995), with a \( U_{\text{eff}} \) for the U atoms of 4.0 eV (\( U_{\text{eff}} = U - J \), with \( U = 4.0 \text{ eV} \), and \( J = 0.0 \text{ eV} \)). The \( U_{\text{eff}} \) value was chosen to be close to that obtained from related experimental results for UO2 (Schoenes, 1987; Kotani and Takao, 1992). The valence electron configurations were [U] 6s²6p⁶5f⁶6d¹7s², [Cs] 5s²5p⁶6s¹, [P] 3s²3p³, [O] 2s²2p⁴, and [F] 2s²2p⁴, respectively.

In an effort to understand why Rb forms an oxyfluoride while Cs only an oxide, we also considered the two opposite
TABLE 1 | Crystallographic details of structures 1-4.

| Formula | Cs$_{11}$(UO$_2$)$_{12}$(PO$_4$)$_3$O$_{13}$ | Rb$_{11}$(UO$_2$)$_{12}$(PO$_4$)$_3$O$_{12}$F$_2$ | Cs$_{4.4}K$_0.6(UO$_2$)$_6$(O$_4$)F(PO$_4$)$_4$(UO$_2$) | Rb$_{4.4}$K$_0.6$(UO$_2$)$_6$(O$_4$)F(PO$_4$)$_4$(UO$_2$) |
|---------------------|-----------------------------|-----------------------------|-----------------------------|-----------------------------|
| S. G. | Prima | Prima | Fdd2 | Fdd2 |
| a, Å | 14.9661(3) | 14.1258(3) | 25.8529(6) | 25.6593(5) |
| b, Å | 17.9863(4) | 18.0121(4) | 28.9286(5) | 27.5792(5) |
| c, Å | 20.8520(4) | 20.6241(4) | 9.32341(2) | 9.2591(2) |
| V, Å$^3$ | 16303.1(2) | 15274.0(19) | 11004.6(3) | 16552.3(2) |
| Crystal size (mm$^3$) | 0.01 x 0.05 x 0.06 | 0.01 x 0.05 x 0.06 | 0.01 x 0.04 x 0.06 | 0.01 x 0.02 x 0.05 |
| Temperature (K) | 300 | 301 | 300 | 300 |
| Density (g cm$^{-3}$) | 6.158 | 5.944 | 5.671 | 5.549 |
| $\theta$ range (°) | 2.381–36.355 | 2.445–36.355 | 2.446–36.355 | 2.452–36.343 |
| $\mu$ (mm$^{-1}$) | 41.774 | 47.232 | 37.649 | 41.374 |
| Unique reflections | 13924 | 13063 | 8388 | 8388 |
| $R_{int}$ | 0.0485 | 0.0467 | 0.0401 | 0.0410 |
| $\Delta R_{max}$ (Å$^{-3}$) | 3.422 | 3.152 | 2.072 | 1.773 |
| $\Delta F_{min}$ (Å$^{-3}$) | -5.467 | -3.117 | -2.471 | -2.325 |
| $\sigma$ | 1.111 | 1.128 | 1.141 | 1.081 |
| Extinction coefficient | 0.000068(2) | 0.000011(2) | - | - |
| $R_1(F)$ for $F_0^2 > 2\sigma(F_0^2)$ | 0.0262 | 0.0278 | 0.0191 | 0.0179 |
| $R_w(F_0^2)$ | 0.0473 | 0.0551 | 0.0379 | 0.0402 |

Cases, Rb$_{11}$(UO$_2$)$_{12}$(PO$_4$)$_3$O$_{13}$ and Cs$_{11}$(UO$_2$)$_{12}$(PO$_4$)$_3$O$_{12}$F$_2$. Because the oxide and oxyfluoride compounds have different composition, we cannot directly compare their calculated total energies, i.e., thermodynamic stability. Therefore, we need to investigate their relative stability by analyzing the reaction enthalpies, $\Delta_r H$, considering the two reactions:

$$12\text{UF}_4 + 3\text{AlPO}_4 + 11\text{RbCl} + 37/2\text{O}_2 \rightarrow \text{Rb}_{11} (\text{UO}_2)_{12} (\text{PO}_4)_3 \text{O}_{12} \text{F}_2 + 3\text{AlF}_3 + 37/2 \text{F}_2 + 11/2 \text{Cl}_2 \quad (1)$$

$$12\text{UF}_4 + 3\text{AlPO}_4 + 11\text{CsCl} + 37/2\text{O}_2 \rightarrow \text{Cs}_{11} (\text{UO}_2)_{12} (\text{PO}_4)_3 \text{O}_{13} + 3\text{AlF}_3 + 39/2 \text{F}_2 + 11/2 \text{Cl}_2 \quad (2)$$

The $\Delta_r H$ values were calculated using:

$$\Delta_r H = \sum_{i=products} c_i \Delta_f H (i) - \sum_{j=reactants} c_j \Delta_f H (j), \quad (3)$$

where $\Delta_f H$ are the formation energies per formula unit of the products, $i$, and reactants, $j$, and the sum is over all products and reactants. $c_i$ and $c_j$ are the stoichiometric coefficients of the products and reactants, respectively. For each of the reactants and products we calculated their $\Delta_f H$ using the same VASP calculations input parameters listed above.

DFT gives only the reaction enthalpy at 0 K, and to include the temperature effect on the reactions, we calculate the finite temperature quasi-Gibbs formation energies, $f g$, using the equation:

$$\Delta fg = \Delta f H - TS\text{conf} \quad (4)$$

$S\text{conf}$ is the configurational entropy, defined as:

$$S\text{conf} = k_b \sum x_i \ln (x_i) \quad (5)$$

where $k_b$ is the Boltzmann constant, $x_i$ is the mole fraction of the constituent $i$, and the sum is over each constituent $i$ in the compound. Note that in our calculations we do not consider the vibrational contribution to the entropy because due to their very large size, calculating this term for the title compounds is outside the current capabilities of DFT, and hence the term quasi-Gibbs energy. In the case of the gases $\text{O}_2$, $\text{F}_2$, and $\text{Cl}_2$, we use tabulated values for the standard entropies (Chase, 1998).

**DISCUSSION**

**Synthesis**

There have been numerous reported uranium phosphate containing structures prepared by similar synthetic methods...
using UF₆, AlPO₄, and alkali chloride fluxes, predominantly loaded into alumina crucibles and heated at a temperature of 875°C (Juillerat et al., 2018a,b; Juillerat and zur Loye, 2019; Juillerat et al., 2019b). Cs₁₅(UO₂)₁₂(PO₄)₃O₁₃ (1) and Rb₁₁(UO₂)₁₂(PO₄)₃O₁₂F₂ (2) were first discovered as the minor product, previously unidentified red tablets, in the synthesis of Cs₆[(UO₂)₃O₄(PO₄)₁₄] and Rb₆[(UO₂)₃O₄(PO₄)₁₄], respectively (Juillerat et al., 2018b). The optimization of the Cs containing analog lead to the use of platinum crucibles, and was successful, but when using analogous synthetic techniques for the Rb analog, only simple rubidium oxides, such as Rb₂U₂O₇, were obtained in platinum crucibles. The use of alumina crucibles for the synthesis of Rb₁₁(UO₂)₁₂(PO₄)₃O₁₂F₂ (2) proved necessary, although the reason is not well-understood. Structures 3 and 4, related to the phosphuranylite topology, were discovered when trying to optimize synthetic conditions for Cs₁₄K₂₆[(UO₂)₂O₂(PO₄)₁₂] and Cs₁₇K₄₃[(UO₂)₃O₅(PO₄)₁₂], respectively (Juillerat et al., 2018a). The title phases, Cs₈₄K₄₆[(UO₂)₆O₂F(PO₄)₁₂(UO₂)] (3) and Rb₄₄K₄₆[(UO₂)₆O₂F(PO₄)₁₂(UO₂)] (4) were obtained simultaneously with Cs₁₄K₂₆[(UO₂)₃O₂(PO₄)₁₂] and Rb₁₄K₂₆[(UO₂)₃O₂(PO₄)₁₂] by further reducing the flux to reactants to 10 mmol and 5 mmol of flux with 0.5 mmol UF₆; unfortunately, the title compounds could not be separated manually from Cs₁₄K₂₆[(UO₂)₂O₂(PO₄)₁₂] and Rb₁₄K₂₆[(UO₂)₂O₂(PO₄)₁₂], as all crystallize as yellow plates.

Structure

CS₁₅[(UO₂)₁₂(PO₄)₃O₁₃] (1) and Rb₁₁[(UO₂)₁₂(PO₄)₃O₁₂F₂] (2) are two dimensional sheet structures (Figure 2C) and crystallize in the orthorhombic space group Pnma with lattice parameters

\[
a = 14.9561(3), \quad b = 17.9663(4), \quad c = 20.8520(4), \quad a = 14.1258(3), \quad b = 18.0121(4), \quad c = 20.6241(4)
\]

respectively. To our knowledge, the sheet topology present in both structures is unreported in the literature and can be deconstructed into units of the ß-U₃O₈ topology as shown in Figure 2A. The ß-U₃O₈ topology can be deconstructed into U₃O₁₆ and U₂O₁₄ units, where the U₃O₁₆ unit is a square bipyramid, edge-sharing with two pentagonal bipyramids on either side, and the U₂O₁₄ unit is a corner-sharing pentagonal bipyramid. These two units alternate to form the ß-U₃O₈ topology as shown in Figure 2A. Structure 1 is also built-up of alternating U₃O₁₆ and U₂O₁₄ units and 2 contains the U₃O₁₆, U₃O₁₄, and U₂O₁₃F units where the pentagonal bipyramids corner share through the F; however, every third U₃O₁₆ unit is missing in both structures (Figure 2B).

Between the group of four pentagonal bipyramids (two edge sharing U₂O₁₄ or U₂O₁₃F units) is a disordered phosphate tetrahedra with two possible orientations as shown in Figure 2D. Additional phosphate tetrahedra edge share with the U₂O₁₄/U₂O₁₃F units that are located between two U₃O₁₆ units and corner share to the adjacent group of four pentagonal bipyramids. The disorder in the phosphate tetrahedron, P₃ in both structures 1 and 2, is slightly different between the two structures as shown in Figure 3. In Figure 3A, depicting Rb₁₄[(UO₂)₁₂(PO₄)₃O₁₂F₂] (2), the phosphate tetrahedron is half occupied and accompanied by a split oxygen fluorine site whose occupations sum to 1. Therefore, either the phosphate tetrahedron points up or down (with respect to the plane of the sheet), the oxygen site corresponds to the orientation of the phosphate tetrahedron, and the fluorine site corresponds to the absence of the phosphate tetrahedron. This is supported by the P₃-O₂₈A and P₃-F₂₈B bond distances which are 1.558(5) and 2.170(8) Å, respectively where the P-F bond is much too long for the tetrahedral coordination environment of P⁵⁺. Tables of bond valences and bond distances for U and P for all structures are collected in Tables S1–S4.

The disorder in the P₃ tetrahedron in the Cs analog, structure 1, is similar by virtue of the phosphate tetrahedron pointing up or down within the plane of the sheet; however, the electron density near the O₂₈ site freely refines to a half occupied oxygen site (rather than unity as in 2), and therefore in the absence of the phosphate tetrahedron there are two square bipyramids (Figure 3B) as opposed to two corner-sharing pentagonal bipyramids as in 2. The bond valence sums of U₆ and U₇, the corner-sharing pentagonal bipyramids in 2 and the two square bipyramids created by the absence of P₃ in 1, are slightly lower at values of 5.749 and 5.767, respectively, for 1, as compared to 5.844 and 5.833, respectively for 2; however, all values are within the accepted range for U⁺⁺ (~5.6–6.1) (Burns et al., 1997). Tables of bond valences and bond distances for U and P for all structures are located in Tables S1–S4.

While EDS identifies the presence (or absence) of fluorine in structures 1 and 2, it does not identify the positions of the fluorine sites within structure 2. In order to locate the F sites in 2 we calculated BVS for all possible F sites, which includes all oxygen sites coordinated to the uranium sites except for the axial uranyl oxgens, as F on a uranyl oxygen site would be extremely unexpected given the bond order of the ~1.8 Å U-O “y” bond (3) and multiple bonds are not possible for F. All of the uranyl U-O bond lengths in 2 are between 1.802(4) and 1.830(6) Å and show no significant deviation from the expected ~1.8 Å bond length. Bond valence sums of the remaining O atoms are between 1.82 and 2.30 using rₒ = 2.051 and B = 0.519 for U-O (Burns et al., 1997), rₚ = 1.617 and B = 0.370 for P-O (Brown and Altermatt, 1985), and rₒ = 2.081 and B = 0.515 for Rb-O (Brown and Altermatt, 1985), except for “OS” and “O₂BB” which have low values of 1.42 and 1.28, and which are significantly lower.
than the expected value of 2. If $r_0 = 1.98$ and $B = 0.40$ for U-F bonds (Zachariasen, 1978), these bond valence sums come out to 1.02 and 0.94, respectively, and match well with the expected value of 1 for F; therefore, these sites have been identified as F5 and F28B and are necessary for achieving charge balance in the structure. For comparison, the bond valence sums for O5 and O28 sites in structure 1, that contains no fluorine, are 1.86 and 1.90, respectively, and therefore these results also support our decision to assign the fluorine sites in 2 as F5 and F28B.

\[
\text{Cs}_{4.4}\text{K}_{0.6}[(\text{UO}_2)_6\text{O}_4\text{F}(\text{PO}_4)_4]\text{(UO}_2\text{)] \quad (3)
\]

and

\[
\text{Rb}_{4.4}\text{K}_{0.6}[(\text{UO}_2)_6\text{O}_4\text{F}(\text{PO}_4)_4]\text{(UO}_2\text{)] \quad (4)
\]

also contain small amounts of fluorine as identified by EDS and by the need for charge balance in the structures. Similar methods as described above were used to identify the fluorine sites(s), again excluding uranyl oxygen sites as possibilities; however, the results are less definitive than the bond valence sums of 2. In 3 all O bond valence sums are between 1.92 and 2.22, none of which signal good candidates for fluorine doping, and similarly in 4, the O BVS are between 1.78 and 2.25. This suggests that there is no preferred site for F and for this reason we have arbitrarily set the occupancy of O3 to be half occupied by both F and O, as this site has the lowest BVS in both structures 3 and 4, and the rarity of PO$_3$F tetrahedra leaves O3 and O6 as the most plausible options. [(UO$_2$)$_3$(HPO$_4$)$_3$(PO$_4$)$_4$](H$_2$C$_{10}$N$_2$)$_3$ synthesized hydrothermally using PF$_6^-$ as the F$^-$ source also contains phosphuranylite related layers and fluorine is present on sites similar to the ones found in 3 and 4 (Deifel et al., 2008).

The Cs$_{4.4}$K$_{0.6}[(\text{UO}_2)_6\text{O}_4\text{F}(\text{PO}_4)_4]\text{(UO}_2\text{)] \quad (3)
\]

and

\[
\text{Rb}_{4.4}\text{K}_{0.6}[(\text{UO}_2)_6\text{O}_4\text{F}(\text{PO}_4)_4]\text{(UO}_2\text{)] \quad (4)
\]

structures are similar to the phosphuranylite mineral, KCa(H$_3$O)$_3$[(UO$_2$)$_6$O$_4$(PO$_4$)$_4$(UO$_2$)(H$_2$O)$_8$] (Demartin et al., 1991), as they contain the same phosphuranylite-type layers constructed of chains of alternating UO$_8$ and U$_2$O$_{12}$ units connected to adjacent chains through corner- and edge- sharing phosphate tetrahedra (Figure 4A). There is also an additional uranium site, square bipyramid, corner sharing with four phosphate tetrahedra to link adjacent sheets, as there is in phosphuranylite (Figure 4B). The alkali sites fill the voids between the uranyl phosphate layers (Figures 4D,E). Several recent papers have further characterized phosphuranylite type layers by the direction in which the phosphate tetrahedra point (up or down orthogonal to the plane of the sheet) and there...
are seven known isomers (Locock and Burns, 2003; Juillerat et al., 2018a; Juillerat and zur Loye, 2019). Both structures 3 and 4 are the uudduuO isomer, observed in the mineral phurcalite (Atencio et al., 1991), while phosphuranylite is the uudduuS isomer. In addition to the presence of fluorine in the uranyl phosphate sheets, the stacking of the uranyl phosphate sheets in 3 and 4 is also different from those observed in other phosphuranylite based structures. In phosphuranylite and recently reported phosphuranylite type structures, the chains of UO$_8$ and U$_2$O$_{12}$ units in adjacent sheets run parallel to each other, while in 3 and 4 there are two orientations of these chains that alternate between layers, where the torsion angle between chains in two adjacent layers is 37.8°. This is illustrated in Figure 4C where parallel layers are shown in yellow, and the layer between these is shown in orange.

**First-Principles Calculations**

As was mentioned previously, Cs prefers to form the oxide structure, while Rb prefers the oxyfluoride structure, and to understand the cause of this different behavior, we studied their reaction enthalpies using DFT. Shown in Table 2 are the calculated $\Delta_rH$ values which indicate reactions (1) and (2) are thermodynamically unfavorable, i.e., their $\Delta_rH$ values are positive. Also, the [A, O$_{12}$F$_2$] compounds have more negative $\Delta_rH$ compared to the respective [A, O$_{13}$] compound, indicating that forming the [A, O$_{12}$F$_2$] is preferred over the [A, O$_{13}$]. Experimental results confirm that this is the case for the Rb containing compound, it disagrees for that containing Cs. This discrepancy between experiment and calculations may come from the fact that the calculations are performed at 0 K, and thus, finite temperature enthalpy values could provide a different conclusion.

To consider the temperature effect, we calculated the $r_g$ using Equation (4), and substituted them in Equation (3) to obtain the quasi-Gibbs reaction energies, $r_g$. Shown in Figure 5 is the calculated $r_g$ as a function of the temperature. With increasing temperature the $r_g$ becomes more negative, eventually becoming $<0$ at $T > 2,200$ K, implying that above that temperature the reactions are thermodynamically favorable. It is also important to note that the $r_g$ of the [Cs, O$_{13}$] compound becomes more negative than the $r_g$ of the [Cs, O$_{12}$F$_2$] compound for $T > 1,900$ K, the temperature at which a phase change occurs. Moreover, above the temperature at which the $r_g$ becomes negative, the [Cs, O$_{13}$] $r_g$ is more negative compared to the [Cs, O$_{12}$F$_2$] $r_g$, indicating that above 2,200 K the formation of [Cs, O$_{13}$] is thermodynamically preferred over the formation of [Cs, O$_{12}$F$_2$]. The results suggest that the formation of the oxide is driven by the entropy, and that at high enough temperatures, above 2,925 K from our calculations, the [Rb, O$_{13}$] can also be formed over the [Rb, O$_{12}$F$_2$]. Also, note that the difference between the phase change temperatures of the Cs and Rb compounds is 1,025 K, which is big enough so that a phase change is observed in one case but not the other. However, the calculated reaction temperature, $\sim 2,200$ K is much higher than the experimental one, 1,148 K. The difference arises from the absence of the other entropic contributions in our calculations,

![Figure 3](image-url)
FIGURE 4 | (A) The phosphuranylite layers found in 3 and 4. (B) The phosphuranylite layers plus the square bipyramid uranyl sites and alkali cations. (C) Depiction of the 37.8° torsion angle between chains in adjacent layers. (D) View of 3 in the c direction and (E) view of 4 in the c direction. Uranium, phosphate, and oxygen are shown in yellow, magenta, and red, respectively. Alkali cations are shown in blues, where blurred spheres represent partially occupied disordered sites, and the half light/dark blue spheres represent the Cs/K and Rb/K shared sites.

TABLE 2 | Reaction enthalpies (Δ_rH) and difference in reaction enthalpies (Δ_Δ_rH), in kJ/mol/atom, of the A_11(UO_2)_{12}PO_4O_{12}F_2 [A, O_{12}F_2] and A_11(UO_2)_{12}PO_4O_{13} [A, O_{13}] compounds (A = Rb, Cs).

| A_11 | [A, O_{12}F_2] | [A, O_{13}] | Δ_Δ_rH ([A, O_{13}] – [A, O_{12}F_2]) |
|------|----------------|-------------|-------------------------------------|
| Rb   | 47.02          | 53.90       | 6.88                                |
| Cs   | 47.14          | 51.23       | 4.09                                |

except for the gases. Because of the large size of the systems we are not able to calculate the phonon spectra, whereas introducing the vibrational contribution might lower the calculated reaction temperature to better match the experimental results.

**Ion Exchange**

The ion exchange products of 1 soaked in RbCl and KCl and 2 soaked in CsCl show small changes in the PXRD patterns shown in Figures S1, S2, indicating the layered structures are maintained throughout the ion exchange process. EDS was used to qualitatively analyze the alkali contents of each sample before and after ion exchange. The results showed that after 3 days of soaking in concentrated salt solution approximately half of the alkali species are exchanged. In the exchange of Cs in 1 for Rb and K, the approximate contents of the post ion-exchange products are 5.3 Cs, 5.7 Rb, and 5.4 Cs, 5.6 K, respectively. While in the exchange of Rb for Cs in 2, results in 6.3 Rb, 4.7 Cs.

**Optical Properties**

The UV-vis absorption spectra (Figure S3) and fluorescence emission spectra (Figure S4) of Cs_11(UO_2)_{12}(PO_4)_{3}O_{13} (1) and Rb_11(UO_2)_{12}(PO_4)_{3}O_{12}F_2 (2) are typical of U^6+ species in uranium oxide extended structures. 1 and 2 absorb broadly from 200 to 575 nm and can be classified as semiconductors. A careful look at the DFT calculated density of states (Figure S5)
showed that these compounds are actually Mott insulators. The ligand to metal charge transitions are at 377 and 379 nm, respectively and the transitions from the $\text{UO}_2^{2+}$ core are at 473 and 463 nm, respectively. The maximum fluorescence emission occurs at an excitation wavelength of 437 nm where the emission peak is centered on 574 and 564 nm, respectively for 1 and 2.

**CONCLUSIONS**

Three new uranyl phosphate oxyfluorides, and one uranyl phosphate, have been synthesized by molten flux methods using alumina crucible reaction vessels and alkali chloride fluxes. Their structures were determined by SXRD and the presence of fluorine was confirmed by qualitative EDS. The location of the fluorine sites was deduced using bond valence sums, powder X-ray diffraction data, PXRD, DFT calculations, ion-exchange experiments, and optical spectroscopy. The DFT calculations support the observation of the Rb, oxyfluoride structures (2) in contrast to the pure Cs, oxide structure of (1), indicating that the formation of pure oxide structure may be driven by entropy, and it might be obtained for both Rb and Cs, given high enough temperatures. The temperature difference in the temperatures at which the pure oxide structures can be obtained is 1,025 K between the Rb and Cs, which hints at the reason why we see an oxyfluoride in the Rb containing (2) and the pure oxide in the Cs (1) containing phases. Structures 1 and 2 are capable of alkali ion exchange, where approximately half of the alkali cations in the parent structure can be replaced by a target alkali species in concentrated salt solutions, although the Cs containing structure, 1, undergoes more extensive ion exchange than the Rb analog, 2, perhaps due to the larger interlayer spacing in 1. Alkali chloride fluxes continue to be a viable synthetic technique for crystallizing new uranium phosphate structures containing new structure types and further exploration should continue, in addition to expanding to alkaline fluxes in order to incorporate divalent cations and hopefully obtain new novel structure types.

**DATA AVAILABILITY**

CCDC deposition numbers 1898442–1898445 contain the supplementary crystallographic data for this paper. These data can be obtained free of charge via www.ccdc.cam.ac.uk/data_request/cif, or by emailing data_request@ccdc.cam.ac.uk, or by contacting The Cambridge Crystallographic Data Center, 12 Union Road, Cambridge CB21EZ, UK; fax: +44 1223 336033.

**AUTHOR CONTRIBUTIONS**

CJ and H-CzL were responsible for the synthesis and structural characterization of the four new compounds and most of the written manuscript. VK and TB contributed the DFT calculations, methods, and discussion.

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**SUPPLEMENTARY MATERIAL**

The Supplementary Material for this article can be found online at: https://www.frontiersin.org/articles/10.3389/fchem.2019.00583/full#supplementary-material

An extended discussion of the crystallographic refinements of 1 and 2, additional details on the DFT calculations, bond valence sums and selected bond distances, powder X-ray diffraction data, optical spectra of 1 and 2, and DFT calculated density of states can be found in the Supporting Information.
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Conflict of Interest Statement: The authors declare that the research was conducted in the absence of any commercial or financial relationships that could be construed as a potential conflict of interest.

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