Angular Sizes and Effective Temperatures of O-type Stars from Optical Interferometry with the CHARA Array

Kathryn D. Gordon¹, Douglas R. Gies¹, Gail H. Schaefer², Daniel Huber³, Michael Ireland⁴, and D. John Hillier⁵
¹ Center for High Angular Resolution Astronomy and Department of Physics and Astronomy, Georgia State University, P. O. Box 5060, Atlanta, GA 30302-5060, USA; kgordon@astro.gsu.edu
² The CHARA Array of Georgia State University, Mount Wilson Observatory, Mount Wilson, CA 91023, USA
³ Institute for Astronomy, University of Hawai‘i, 2680 Woodlawn Drive, Honolulu, HI 96822, USA
⁴ Research School of Astronomy & Astrophysics, Australian National University, Canberra, ACT 2611, Australia
⁵ Department of Physics and Astronomy and Pittsburgh Particle Physics, Astrophysics, and Cosmology Center (PITT PACC), University of Pittsburgh, Pittsburgh, PA 15260, USA

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Abstract

We present interferometric observations of six O-type stars that were made with the Precision Astronomical Visible Observations beam combiner at the Center for High Angular Resolution Astronomy (CHARA) Array. The observations include multiple brackets for three targets, λ Ori A, ζ Oph, and 10 Lac, but there are only preliminary, single observations of the other three stars, ζ Per, α Cam, and ζ Ori A. The stellar angular diameters range from 0.55 mas for ζ Ori A down to 0.11 mas for 10 Lac, the smallest star yet resolved with the CHARA Array. The rotational oblateness of the rapidly rotating star ζ Oph is directly measured for the first time. We assembled ultraviolet to infrared flux measurements for these stars, and then derived angular diameters and reddening estimates using model atmospheres and an effective temperature set by published results from analysis of the line spectrum. The model-based angular diameters are in good agreement with those observed. We also present estimates for the effective temperatures of these stars, derived by setting the interferometric angular size and fitting the spectrophotometry.

Key words: stars: early-type – stars: fundamental parameters – stars: massive – techniques: interferometric

Supporting material: machine-readable table

1. Introduction

The fundamental properties of early O-type stars, such as mass, radius, and temperature, are the essential parameters required to place stars in the Hertzsprung–Russell diagram for comparison with stellar evolutionary tracks. The derivation of these quantities is usually reserved to members of eclipsing binary stars in which combined radial velocity and photometric light curve analysis can yield estimates of mass and radius (Torres et al. 2010). However, some of these systems probably interacted at some point in their evolution, and comparisons of their properties with evolutionary tracks for single stars may not be entirely reliable. Instead, most of the work on the fundamental parameters of individual O-type stars is based on analysis of the line spectrum, in which the temperature and gravity are derived from the He line ionization balance and the pressure broadening of the hydrogen lines. These studies rely upon detailed atmospheric models that must take into account non-local thermal equilibrium (non-LTE) populations, line-blanketing, and spherical winds. FASTWIND (Santolaya-Ray et al. 1997; Puls et al. 2005), TLUSTY (Hubeny & Lanz 1995), and CMFGEN (Hillier & Miller 1998) are all non-LTE models that can be applied to O-star atmospheres and use different methods to deal with the line-blanketing problem. FASTWIND and CMFGEN also take into account the effects of winds (important in more luminous stars) while TLUSTY does not. These studies are often used to calibrate the MK-classifications of O-stars in terms of temperature and gravity (Martins et al. 2005; Holgado et al. 2018). However, although these calibrations serve as a general reference to connect the spectral classifications of a given star and its parameters, one has to use them carefully when studying the properties of a specific individual target of interest. For example, Simón-Díaz et al. (2014) applied spectral line fits using FASTWIND models to investigate the effective temperature relation with O-subtype. They found a significant scatter of effective temperatures among O-stars of similar spectral type that is partially due to the variation of log g within the O-dwarf luminosity class.

It is important to test the atmosphere models for O-stars because we now rely upon them so completely. The simplest approach in principle is to determine the stellar effective temperature $T_{\text{eff}}$ from the relationship between the extinction-corrected bolometric flux, angular diameter $\theta$, and effective temperature: $f_{\text{bol}} = \frac{1}{4} \theta^2 \sigma T_{\text{eff}}^4$. This method was pioneered by Hanbury Brown et al. (1974) who used the Narrabri Stellar Intensity Interferometer to measure the angular diameters of 32 stars in the spectral range from O5 to F8 (including two stars considered here). Code et al. (1976) used the early satellite observations of the UV flux of these stars to record their spectral energy distribution (SED) and determine effective temperature. However, there were only three O-type stars in the sample observed by Hanbury Brown et al. (1974), and the great distances of the O-stars made other high angular resolution measurements impossible until now.

Furthermore, there are a number of intrinsic problems in using the flux and angular diameter method that were initially discussed by Abbott & Hummer (1985) and Hummer et al. (1988). The primary issue is that most O-stars radiate a large fraction of their flux in the extreme UV, at wavelengths smaller than the Lyman limit at 912 Å. This part of the spectrum is totally obscured by the local interstellar medium in general, and consequently we must rely upon stellar atmosphere models to predict the flux at short wavelengths. The region of spectrum
we can observe is in the Rayleigh–Jeans tail where the continuum shape is more or less independent of temperature, so that the intrinsic shape of the UV continuum (Massa & Savage 1985) and unreddened optical/IR colors (Martins & Plez 2006) are similar among all O-stars. The second problem is that the flux in the observed part of the spectrum has a gravity dependence. The size of the Lyman jump in the SED depends on the ionization state of H, and the higher ratio of ionized to neutral H atoms among the supergiants results in a smaller Lyman jump and lower ionized to neutral H atoms among the supergiants results in a

measurements to obtain a limb-darkened angular diameter

angle in the sky. In Section 3.1, we show how angular measurements are needed to provide an effective test of models. Angular measurements need to be accurate in order to compare the continuum and line results. The relation between the

angular diameter measurements need to be accurate in order to compare the continuum and line results. The relation between the

Fλ(Teff, log g, Z) = fλ 10^Aλ/2 /θ/2^2,

where Aλ is the extinction (in magnitudes) and θ is the angular diameter (in radians). The monochromatic flux in the Rayleigh–Jeans tail varies with temperature as Fλ ∝ Teff, so for a given observed monochromatic flux and extinction, the derived temperature will vary as Teff ∝ θ^-2 and the fractional uncertainty will be ∆Teff /Teff ≈ 2∆θ/θ. Thus, accurate, sub-milliarcsecond angular measurements are needed to provide an effective test of the spectral predictions of the current generation of atmospheric models.

Here, we present the results of our angular diameter measurements of a sample of six O-type stars. Section 2 discusses the observations, calibration, and reduction methods to obtain the interferometric visibility as a function of baseline and position angle in the sky. In Section 3.1, we show fits of the visibility measurements to obtain a limb-darkened angular diameter θL,D, and in Section 3.2 we collect the available spectrophotometry and make fits of the SED as a function of temperature, angular size, and reddening. In Section 4, we gather distance estimates in order to transform the angular diameters into linear radii, and we compare the angular size derived from interferometry with that from model fits of the continuum flux for published values of effective temperature.

### 2. Observations

The stars in our sample consist of six O spectral type stars ranging from O7.5 to O9. There are two supergiants, two giants, one sub-giant and one dwarf. Table 1 lists the parameters of the objects. The effective temperature Teff given in column 8 is the average of the recently published values that are gathered in Table 2. The gravity log g listed in column 9 is likewise the average from those papers noted in Table 2.

Four of the six O stars observed have close companions reported from speckle, adaptive optics, and other studies listed in the Washington Double Star Catalog. Parameters of the companions are shown in Table 3. Most of these companions are faint and have separations greater than the interferometric field of view of 1″, so their flux has no influence on our interferometric data. The exception is the close companion to ζ Ori A, which is discussed below. The companions will, however, contribute to the net flux measured in the SEDs (with the exception of the negligible contributions from the very faint companions of ξ Per and 10 Lac), and we deal with this complication in Section 3.2 below.

Observations of our targets were made using the Precision Astronomical Visible Observations (PAVO) beam combiner (Ireland et al. 2008) at the CHARA Array (ten Brummelaar et al. 2005), located at Mount Wilson Observatory in California. The CHARA Array is an optical interferometer composed of six 1 m telescopes arranged in a Y-shaped configuration. Combinations of the telescopes allow for 15 different usable baselines ranging in length from 34 to 331 m. Combining the longest usable baseline currently available in the world and the operating wavelength range of the PAVO beam combiner (650–800 nm), we were able to achieve an extremely high angular resolution for our targets of about 0.2 mas.

The beams from the Array are fed into the PAVO combiner by a set of lenses and mirrors (Ireland et al. 2008; Maestro et al. 2012). The final set is three small movable prisms that guide the beams to the image plane. After being focused in the image plane, the beams pass through a three-hole mask that spatially filters the light (only two beams and two holes are used here).

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**Table 1** Parameters of Target Stars

| Identifier | Star Name | HD Number | Spectral Classification | V (mag) | B − V (mag) | V − K (mag) | Teff (K) | log g (c.g.s.) | V sin i (km s⁻¹) |
|------------|-----------|-----------|------------------------|--------|-------------|-------------|---------|--------------|---------------|
| a          | ξ Per     | 24912     | O7.5 III(n)(f)         | 4.06   | 0.02        | 0.11        | 34.3 ± 0.8 | 3.49 ± 0.12  | 230           |
| b          | α Cam     | 30614     | O9 Ia                  | 4.29   | 0.05        | 0.05        | 29.4 ± 1.0 | 3.03 ± 0.19  | 113           |
| c          | ζ Ori A   | 36861     | O8 III(f)              | 3.47   | 0.01        | −0.56       | 34.5 ± 0.8 | 3.64 ± 0.13  | 59            |
| d          | ζ Ori A   | 37742     | O9.2 Ib                | 1.88   | −0.11       | −0.44       | 29.5 ± 1.0 | 3.25 ± 0.25  | 124           |
| e          | ζ Oph     | 149757    | O9.2 Vm                 | 2.56   | 0.02        | −0.06       | 32.1 ± 1.3 | 3.66 ± 0.13  | 311           |
| f          | 10 Lac    | 214680    | O9 V                   | 4.88   | −0.21       | −0.62       | 35.5 ± 0.5 | 3.97 ± 0.08  | 16            |

**Note.** Effective temperatures and gravities are average values taken from the sources listed in Table 2. Spectral types are from the Galactic O-Star Spectroscopic Survey (Sota et al. 2011). Projected rotational velocities *V sin i* are from Simón-Díaz & Herrero (2014).

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6. [http://ad.usno.navy.mil/wds/](http://ad.usno.navy.mil/wds/)
The beams then interfere and produce fringes that are spatially modulated in the pupil plane. Finally, a lenslet array divides the pupil into 16 segments and a prism disperses the fringes in each segment into 23 or more spectral channels. Throughout a night of observing the alignments of the image and pupil plane are checked for each new target, fringes are found, and adjustments made to optimize the longitudinal dispersion corrector position.

Data for each target were taken using the standard bracket method where one bracket is three scans in order of: calibrator–target–calibrator. Observing in brackets allows the visibilities to be obtained as the square of the visibility of a single star as a function of spectral type, 

\[ \text{vis} = \left| \frac{I_{\text{obs}}}{I_{\text{cal}}} \right| \]

making a polynomial fit of the differential surface brightness of a star as a function of spectral type (Chelli et al. 2016). The JSDC diameters are generally in good agreement with independent estimates from CADARS (Pasinetti Fracassini et al. 2001) and Swihart et al. (2017) (see Table 4). The exception is the calibrator for \( \zeta \) Oph, HD 154445, which has a larger size in the JSDC Catalog. The angular diameter of HD 154445 is given as 0.16 mas by CADARS, 0.18 mas by Swihart et al. (2017), and a spectroscopic study by Lyubimkov et al. (2002) implies a diameter of 0.21 mas. These diameter estimates are all significantly smaller than the JSDC value of 0.28 mas, so we adopted the angular diameter found by Swihart et al. (2017) of 0.18 mas for this calibrator.

Observations of our targets with CHARA were accomplished from 2013 November to 2017 June. For all observations only one baseline, or two telescopes, was used at a time. Observing data, including dates, baselines, and calibrated visibilities, are given in Table 5 (given in full in the online version). Column 4 of Table 5 lists the spatial frequency of the observation, or baseline divided by wavelength. Columns 5 and 6 give the positions in the \( u, v \) plane of spatial frequency for each observation. Column 8 gives the visibility squared and column 9 gives the uncertainty associated with each \( V^2 \) measurement.

### Table 2

Properties from the Literature: \( T_{\text{eff}} \) (kK), \( \log g \) (c.g.s.)

| Source            | \( \xi \) Per | \( \alpha \) Cam | \( \lambda \) Ori A | \( \zeta \) Ori A | \( \zeta \) Oph | 10 Lac | Code       |
|-------------------|---------------|------------------|-------------------|-----------------|--------------|--------|-----------|
| Bouret et al. (2008) | ...           | ...              | ...               | 29.5, 3.25      | ...           | ...    | CMFGEN    |
| Herrero et al. (2002)  | ...           | ...              | 29.4, 2.90        | 35.2, 3.50      | ...           | 35.5, 3.95 | FASTWIND  |
| Holgado et al. (2018)  | ...           | ...              | ...               | ...             | 35.2, 3.90    | FASTWIND | IACOB-GBAT |
| Marcelino et al. (2009) | ...           | ...              | ...               | ...             | 32.0, 3.60    | ...    | TLUSTY    |
| Markova et al. (2004)  | 34.0, 3.35    | 31.0, 3.19       | 33.6, 3.56        | ...             | ...           | ...    | FASTWIND  |
| Martins et al. (2012)  | ...           | ...              | ...               | 29.5, 3.25      | ...           | ...    | CMFGEN    |
| Martins et al. (2015)  | 34.0, 3.60    | 29.5, 3.25       | 35.0, 3.75        | ...             | 31.0, 3.60    | 35.0, 4.05 | CMFGEN    |
| Martins et al. (2017)  | 33.5, 3.50    | ...              | 35.0, 3.75        | ...             | ...           | ...    | CMFGEN    |
| Mokiem et al. (2005)   | ...           | ...              | ...               | ...             | 32.1, 3.62    | 36.0, 4.03 | FASTWIND  |
| Najarro et al. (2011)   | ...           | 28.9, 3.01       | 34.5, 3.70        | ...             | ...           | ...    | CMFGEN    |
| Puls et al. (2006)     | 35.0, 3.50    | 29.0, 3.00       | 33.6, 3.56        | ...             | ...           | ...    | FASTWIND  |
| Repolust et al. (2004)  | 34.0, 3.50    | 29.0, 2.97       | ...               | ...             | 32.0, 3.65    | ...    | FASTWIND  |
| Repolust et al. (2005)  | ...           | 29.0, 2.88       | ...               | ...             | 33.5, 3.85    | ...    | FASTWIND  |
| Simón-Díaz et al. (2006)| ...           | ...              | ...               | ...             | ...           | ...    | FASTWIND  |

### Table 3

Companions of Target Stars

| Star Name | Separation (arcsec) | \( \Delta m_V \) (mag) | \( T_{\text{eff}} \) (kK) | \( \log g \) (c.g.s.) | Spectrophotometric Correction | Interferometric Correction |
|-----------|---------------------|-------------------------|---------------------------|-----------------------|-----------------------------|---------------------------|
| \( \xi \) Per | 2.4\(^a\)          | 9.8\(^b\)               | ...                       | ...                   | N                           | N                         |
| \( \lambda \) Ori A | 4.2\(^b\)          | 2.3\(^b\)               | 25.4\(^b\)               | 4.21\(^b\)            | Y                           | N                         |
| \( \zeta \) Ori A | 0.037\(^d\)        | 2.2\(^d\)               | 26.7\(^d\)               | 4.0\(^d\)             | Y                           | Y                         |
| 10 Lac     | 3.6\(^c\)          | 1.9\(^c\)               | 31.0\(^c\)               | 3.8\(^c\)             | Y                           | N                         |

Note. The last two columns indicate if it was necessary (Y = yes, N = no) to make corrections to the spectrophotometric or interferometric fits due to the companions.

\(^a\) Turner et al. (2008).

\(^b\) Lyubimkov et al. (2004).

\(^c\) Typical values for a B1 IV star (Hummel et al. 2013).

\(^d\) Typical values for a B1 III star (Hummel et al. 2013).

\(^e\) Typical values for a B0 III star (Hummel et al. 2013).

The JSDC diameters are listed in Table 4 and are estimated by making a polynomial fit of the differential surface brightness of a star as a function of spectral type (Chelli et al. 2016). The JSDC diameters are generally in good agreement with independent estimates from CADARS (Pasinetti Fracassini et al. 2001) and Swihart et al. (2017) (see Table 4). The JSDC value of 0.28 mas, so we adopted the angular diameter found by Swihart et al. (2017) of 0.18 mas for this calibrator.
The data were reduced using the standard data reduction and fitting pipeline written for use with the PAVO instrument (Ireland et al. 2008; Maestro et al. 2012). This pipeline first takes the raw data through a routine that allows for the rejection of bad data frames. This allows the user to make cuts based on values of signal-to-noise ratio and loss of lock on fringes. The data undergo background subtraction and photon-bias subtraction, with foreground frames, ratio frames, and dark frames taken during a shutter sequence that runs after fringe data are saved. During a foreground frame all shutters are open but fringe tracking is turned off, and during a ratio frame only one shutter is left open at a time. The processed data are then sent through a second routine that calculates the projected baseline vectors for each observation, calibrates the brackets, and outputs the calibrated visibilities. This routine allows the user to define estimates and uncertainties on the calibrator diameters, as well as provide a limb-darkening coefficient for a linear limb-darkening law.

We generally assume spherical symmetry for the targets so that the angular diameter is independent of the position angle of the baseline projected on the sky. However, ζ Oph is a special case as it is very rapidly rotating with a projected rotational velocity $V \sin i = 348 \text{ km s}^{-1}$, and it will have a rotationally distorted shape. We observed ζ Oph on two nearly orthogonal baselines to obtain a range in ($u, v$) coverage and to ascertain the angular size at different position angles across the star. The target ζ Ori A has a close companion with an orbit measured by Hummel et al. (2013), and the predicted angular separation was 33 mas at the time of our observation with a V-band magnitude difference of 2.2 mag. This companion is close enough and bright enough to contribute extra light and a periodic modulation to the observed visibility measurements.
which, if not accounted for, will make the fitted angular size incorrect. The companion flux was taken into account in our interferometric and spectrophotometric fitting of the ζ Ori A measurements. Using our knowledge of the position of the companion based on the measured orbit, we computed a binary model to fit the visibilities (see Section 4.1).

3. Stellar Parameters

3.1. Interferometry

The visibility measurements we obtained for each star from our interferometric observations were fitted with a single-star, limb-darkened disk model. Linear limb-darkening coefficients in the R-band were interpolated from the tables available in Claret & Bloemen (2011) using the stellar parameters given in Table 1. These limb-darkening coefficients were calculated for model atmospheres that adopt a solar metallicity and a microturbulent velocity of 2 km s⁻¹, and they were derived to maintain flux conservation. The effect of limb darkening is minimal in O-type stars and any uncertainty in the fitted size due to uncertainty in the adopted limb-darkening coefficient will be much smaller than our other sources of uncertainty discussed below. Figures 1 and 2 show the visibility measurements for each star plus an error-weighted fit of all the data with a limb-darkened disk model. Table 6 lists the derived uniform disk (UD) and limb-darkened (LD) disk angular diameters θ, the latter calculated for a linear limb-darkening coefficient μ.

The fitting scheme assigned an uncertainty to the angular diameter based upon the size of the residuals to the fit. However, multiple-night observations of stellar diameters with PAVO show an external night-to-night scatter that is larger than indicated by the uncertainty from measurements within a night by about 5% (Maestro et al. 2013). We checked this inter-night variation with larger sample of 25 B stars observed with the CHARA Array (to be presented in a forthcoming paper) and found the average error to be consistent with the 5% quoted by Maestro et al. (2013) for the PAVO data. Thus, we applied a 5% night-to-night scatter to our error budget. The other source of uncertainty is related to the diameters of the calibrator stars. Because some of our targets are very small (only 0.11 mas for 10 Lac), the calibrator stars may have sizes comparable to the targets. These calibrators can still be used in the analysis but the error in their sizes will play a much bigger role in the error budget than is usually the case where the calibrators are much smaller than the corresponding targets. To account for this effect we fit the data for each star after adjusting the calibrator sizes by plus and minus 1σ, and then derived the range in the solutions. The final uncertainties given in Table 6 are the quadratic sum of the uncertainties from the internal fit uncertainties, the night-to-night external error, and the half-range from varying the calibrator size.

The observations from different nights were not averaged for ζ Oph as there is a true physical difference in size measured along different baselines due to the star’s rotational distortion. The results in Table 6 show that the angular size varies by 15% between the S2W1 and S2E2 baselines. Below in Section 4.1 we present an ellipsoidal fit of the angular diameter as a function of position angle.

3.2. Spectrophotometry

The goal of our spectrophotometric analysis was to compare our results from directly measured angular sizes and observed spectra to predictions of parameters from a stellar atmospheric model. Given the spectral flux across a wavelength range and an estimate of the stellar effective temperature Tₑff from spectral line studies, the models can predict what the angular size should be. We can then compare this against our interferometrically determined angular sizes to test the consistency of model line and flux predictions.

We used fluxes from multiple sources for our targets to create SEDs that span the wavelength range from UV to IR. Sources used for each part of the spectrum are given in Table 7. UV spectra obtained from the International Ultraviolet Explorer (IUE) satellite were recalibrated with a routine by Massa & Fitzpatrick (2000) to correct the flux values. Longer-wavelength IR fluxes were omitted for the supergiant and giant O-stars because their winds create an excess flux in the far-IR that is absent from models without winds. We rebinned the UV and optical spectra to a low resolving power of R = λ/Δλ = 60 on a log λ grid in order to better balance the sampling across the whole spectrum. All flux values in the spectra were assigned a uniform 3% error to ensure our fitting program fit all points equally and did not give more weight to any one part of the spectrum. The exception to this was the case of 10 Lac, a target which has very good data available in the UV and optical from HST/STIS (Bohlin et al. 2017). The errors on these flux values were lower than 3% and the original error values were used for the fitting.

The spectra were compared to the TLUYST OSTAR2002 stellar atmosphere models which adopt solar metallicity and a microturbulent velocity of 10 km s⁻¹ (Hubeny & Lanz 1995; Lanz & Hubeny 2003). Our fitting routine used a grid search method to fit the SED using three parameters: limb-darkened angular size (θ₁LD), effective temperature (Tₑff), and reddening (E(B − V)). For any given set of parameters, a spectrum was extracted from the O-star grid through interpolation in Tₑff and log g (the latter from the adopted gravity given in Table 1). The model spectrum was rebinned to R = 60 in the same way as the observed SED, and then the fluxes were attenuated for interstellar extinction using the IDL Code fnncurve.pro for a ratio of total-to-selective extinction of 3.1 (Fitzpatrick 1999). Adopting an R value greater than 3.1 would result in the model fit predicting a larger angular diameter. Recent extinction fits by Maíz Apellániz & Barbá (2018) give an R value close to 3.1 for all our stars with the exception of α Cam with R = 4.0. Finally the model spectra were rescaled according to the assumed angular diameter and interpolated to the observed wavelength points for direct comparison with the observed SED.

In cases where there was a close, bright companion (Table 3), the extra flux from the companion was included in our fitting. The effective temperature and surface gravity of the companion were used to calculate a model companion spectrum in the same way as above using either the TLUYST OSTAR2002 (Lanz & Hubeny 2003) or BSTAR2006 models (Lanz & Hubeny 2007), depending on the temperature of the companion. The companion flux was then rescaled according to the V-band magnitude difference ∆mᵥ (Table 3) and added to the model flux calculated for the primary. This combined flux spectrum was then used for spectrophotometric fitting of the observed SED.

We began the SED modeling process by creating a grid of angular size and effective temperature, the latter over a range and step size chosen to match the models in the TLUYST grid.
For each pair of $\theta$ and $T_{\text{eff}}$, models were calculated over a grid of reddening values, and the best-fit $E(B-V)$ was found by making a parabolic fit around the reddening grid point with the lowest value of reduced $\chi^2$. The best-fit $E(B-V)$ and $\chi^2$ values were stored in matrices as functions of $\theta_{\text{LD}}$ and $T_{\text{eff}}$.

Contour maps were created by plotting the $\chi^2$ matrix for each star, and these are shown in Figure 3. Overplotted as vertical lines are the angular size obtained from our interferometry with 1$\sigma$ error margins, and horizontal lines show the average temperature from the literature from Table 1 with 1$\sigma$ error margins. The shape of the contours shows that there is generally a valley of low $\chi^2$ where the effective temperature has an inverse square dependence on angular size, as expected from our discussion in Section 1. The contours for the best-fit $E(B-V)$ values (not shown) are parallel lines that follow the curve of the minimum in $\chi^2$ space. Therefore, any temperature and angular size combination chosen along the minimum valley will have a very similar associated $E(B-V)$ value.

We first consider what angular size is predicted from the $\chi^2$ diagrams for estimates of $T_{\text{eff}}$ from published studies of the line
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4. Discussion

4.1. Notes on Individual Stars

ξ Per (HD 24912) is one of three O-type runaway stars in the list (along with α Cam and ζ Oph), and these are usually single stars (Gies & Bolton 1986). The observed angular size is smaller than expected (Table 6; Figure 3); however, given that the measurements are preliminary and that the minimum $\chi^2_\nu$ lies at a diameter only 1.4σ larger than measured, we do not consider the difference significant. The $\chi^2_\nu$ minimum valley has a steep slope in Figure 3, so the derived uncertainty in $T_{\text{eff}}$ is large and we list only an upper limit in Table 8.

α Cam (HD 30614) presents a case where the observed angular size is somewhat larger than expected from model predictions (Table 6), but $\theta_{LD}$ and $\theta_{LD}(T_{\text{eff}})$ agree within the uncertainties.

λ Ori A (HD 36861) represents an example with excellent agreement between $\theta_{LD}$ and $\theta_{LD}(T_{\text{eff}})$ (Table 6). During the data analysis one of the stars used as a calibrator, HD 35149, was found to be a binary and was thus rejected from the calibration process. The final data for λ Ori A are calibrated with only one calibrator star, and the visibilities are slightly more noisy than otherwise expected.

ζ Ori A (HD 37742) has a larger angular size than expected from model predictions (Table 6; Figure 3). The star is the brightest component Aa of a triple system with a close companion Ab, which had a predicted separation of 33 mas at the time of our observations (Hummel et al. 2013). The light from this companion will affect the spectrum and the visibility curve of ζ Ori A, and we accounted for the extra flux of the companion for both the fits of the visibilities and the SED (Section 2). We calculated a binary model for the visibilities, shown in Figure 2, using the predicted position angle, separation, and radius ratio $R/R_\odot = 0.365$ given by Hummel et al. (2013). The model shows fast, low-amplitude oscillations of the visibility curve that are roughly consistent with the observations, and the binary fit yields $\theta_{LD} = 0.556 \pm 0.029$ mas. ζ Ori A was recently observed with the FRIEND beam combiner at the CHARA Array (Martinod et al. 2018) yielding angular diameters of 0.54 ± 0.01 and 0.45 ± 0.12 mas for Aa and Ab, respectively. Their angular diameter measurement agrees within errors with ours for ζ Ori Aa. The estimate of $T_{\text{eff}}$ associated with the observed angular diameter attains a $\chi^2_\nu$ minimum at the lower boundary of the OSTAR2002 grid (Figure 3), so only an approximate upper limit is given in Table 8.

ζ Oph (HD 149757) is a well-known, rapidly rotating star. According to the analysis by Howarth & Smith (2001), it has an equatorial, angular rotational velocity that is 90% of the critical value, and it is viewed in an equatorial orientation with a spin inclination axis angle of 70°. Consequently, its shape should appear oblate due to its rapid rotation. We observed ζ Oph on different baselines with different position angles (S2W1 at −42°:8 and S2E2 at 17°:9) to measure directly this deviation from a perfect sphere. Our measurements were insufficient to make a full ellipsoidal model of the size variation, but we could make a restricted fit by setting the position angle of the rotational axis from earlier polarimetric work. ζ Oph sometimes appears as an Oe star with H Balmer line emission from a circumstellar disk. At the times of observation (2016 July and 2017 June), it did not show Hα emission in its spectra, so it is reasonable to assume that any disk gas has dissipated and we are measuring the angular size of the star itself. However, during a past epoch when a disk was present, Poeckert et al. (1979) used spectropolarimetry to determine the position angle of the disk minor axis as 132.5 ± 6.0 deg east from north. We assume that the circumstellar disk axis is parallel to the stellar rotation axis, so that this is also the position angle of the projected minor axis of the star’s shape. We made a fit of the limb-darkened angular diameter for each $V^2$ measurement, and then we fit an ellipsoid to the diameter as a function of position angle in the sky with the position angle of the minor axis set from the spectropolarimetric result. This gave a major axis of 0.56 mas and a

![Figure 2. Visibility measurements for ζ Ori A with the solid line showing an error weighted single-star fit. An error-weighted binary fit to the visibility data is shown in the inset.](image)
minor ratio of 0.86 is similar to the polar to equatorial radius ratio of 7.5 \( R_p/9.1 \ R_e = 0.82 \) found by Howarth & Smith (2001), although the absolute radii we find are slightly larger because we adopt a larger distance (Table 9). This star is a good target for future interferometric imaging to better determine the rotational distortion and the associated gravity and limb darkening (Che et al. 2011). \( \zeta \) Oph is a runaway star that may have been launched from a supernova explosion in a binary. Its path has been traced back with that of a pulsar that was ejected during the supernova (Hoogerwerf et al. 2000).

10 Lac (HD 214680) has the smallest angular diameter (\( \theta_{LD} = 0.11 \pm 0.02 \) mas) that has been measured with CHARA to date. Because this is below the nominal resolution limit of PAVO of 0.2 mas, we need to check carefully the associated uncertainty of our measurement. Three calibrators were used for the observations of 10 Lac. The fitted angular size is very sensitive to the error in the calibrator size when the target star is smaller in angular size than the calibrator, as in this case. To account for this, we varied each calibrator in size by plus and minus 1\( \sigma \), then refit the data with the new calibrator size. We then took the range between the fits as part of our error budget. This method was subsequently applied to all stars in the sample (Section 3.1). Working close to the resolution limit of PAVO resulted in some non-physical \( (V^2 > 1) \) visibility estimates. We retained these points except in one case where an entire bracket yielded visibilities greater than unity. Both spectroscopic observations and our interferometric results arrive at relatively high effective temperatures, 40.0 kK and 35.5 kK, respectively, which are well above the 31.9 kK temperature associated with its classification of O9 V (Martins et al. 2005). It has been noted in other studies (Simón-Díaz et al. 2014; Holgado et al. 2018) that the \( T_{eff} \) values from the calibrations in Martins et al. (2005) are too low for O9 V stars. However, the extended minimum valley in the \( \chi^2 \) diagram (Figure 3) does encompass the lower temperature (as does the uncertainty region of measured angular diameter).

### Table 6: Angular Diameters

| Star Name | Telescope Pair | \( N_{CL} \) | \( \theta_{UD} \) (mas) | \( \theta_{LD} \) (mas) | \( \theta_{LD(U79)} \) (mas) | \( \theta_{LD(HB74)} \) (mas) | \( \theta_{LD(CADARS)} \) (mas) | \( \theta_{LD(T_{eff})} \) (mas) |
|-----------|----------------|---------|----------------|----------------|----------------|----------------|----------------|----------------|
| \( \zeta \) Per | W1E1           | 23      | 0.216 \pm 0.016 | 0.174          | 0.218 \pm 0.016\* | ...            | ...            | 0.26           | 0.245 \pm 0.010 |
| \( \alpha \) Cam | S1E1           | 23      | 0.250 \pm 0.014 | 0.250          | 0.256 \pm 0.014\* | 0.292 \pm 0.003 | ...            | 0.29           | 0.245 \pm 0.010 |
| \( \lambda \) Ori A | S1E1,W1E1     | 168     | 0.219 \pm 0.015 | 0.253          | 0.226 \pm 0.015 | 0.235 \pm 0.003 | ...            | 0.24           | 0.228 \pm 0.009 |
| \( \zeta \) Ori A | W1E1           | 23      | 0.546 \pm 0.029 | 0.203          | 0.556 \pm 0.029\* | 0.527 \pm 0.010 | 0.48 \pm 0.04   | 0.47           | 0.485 \pm 0.019 |
| \( \xi \) Oph | S2W1           | 69      | 0.454 \pm 0.010 | 0.204          | 0.462 \pm 0.010 | 0.494 \pm 0.003 | 0.51 \pm 0.05   | 0.54           | 0.539 \pm 0.021 |
| \( \xi \) Oph | S2E2           | 161     | 0.532 \pm 0.010 | 0.204          | 0.540 \pm 0.010 | ...            | ...            | 0.13           | 0.121 \pm 0.005 |

Note. \( \* \theta_{UD} \) represents preliminary results that are based upon only a single data bracket. \( N_{CL} \) is the number of visibility measurements. U79 = Underhill et al. (1979), HB74 = Hanbury Brown et al. (1974), CADARS = Pasinetti Fracassini et al. (2001), \( T_{eff} \) = diameter derived from temperature and SED.

### Table 7: Spectrophotometry Sources

| Star Name | Far UV | Near UV | Optical | IR |
|-----------|--------|---------|---------|----|
| \( \xi \) Per | SWP45474 | LWP23809 | SP1     | 2MASS |
| \( \alpha \) Cam | HUT    | LWP17592 | SP2     | 2MASS |
| \( \lambda \) Ori A | OAO    | OAO     | SP1     | 2MASS |
| \( \zeta \) Ori A | SWP33049, SWP33050 | LWP11671, LWP12826 | SP3     | 2MASS |
| \( \xi \) Oph | SWP06776, SWP18252 | LWP12637, LWR14381 | SP1     | 2MASS, WISE, AKARI, Spitzer, IRAS |
| 10 Lac    | SWP*+STIS | HST/STIS | HST/STIS | 2MASS, WISE, AKARI, IRAS |

Note. The UV spectra are primarily from the archive of the IUE (low dispersion, large aperture) where the file number is related to the camera: SWP = short wavelength prime, LWP = long wavelength prime, and LWR = long wavelength redundant. SWP* refers to the average of 52 SWP spectra covering the 1160–1640 Å range. All the fluxes were corrected using the algorithm from Massa & Fitzpatrick (2000). Other UV fluxes are from HUT = Hopkins Ultraviolet Telescope (Buss et al. 1995), OAO = Orbiting Astronomical Observatory 2 (Code & Meade 1979), and HST/STIS from the CALSPEC database (Bohlin et al. 2017). Optical spectrophotometry sources are coded as SP1 = Burnashev (1985), SP2 = Kharitonov et al. (1988), and SP3 = Krisciunas et al. (2017). IR fluxes are from 2MASS (Cutri et al. 2003), WISE (Cutri et al. 2012), AKARI (Ishihara et al. 2010), Spitzer (Ardila et al. 2010), and IRAS (Helou & Walker 1988).

4.2. Consistency with SED Fits from Model Atmospheres

Our primary goal was to test whether the angular diameters, spectroscopically determined temperatures, and SEDs led to a consistent set of stellar parameters. If so, then the intersection of the observed angular diameter (vertical lines) and estimated effective temperature (horizontal line) would cross near the minimum \( \chi^2 \) contours in Figure 3. We find that the angular diameters estimated from the published effective temperatures and fits of the SEDs (\( \theta_{LD(T_{eff})} \)) given in the final column of Table 6) are generally in good agreement with the interferometric angular diameters. A comparison of observed \( \theta_{LD} \) and the predicted angular size \( \theta_{LD(T_{eff})} \) is shown in Figure 5. This figure shows that the average ratio of \( \theta_{LD(T_{eff})} \) to \( \theta_{LD} \) is approximately 0.99 \pm 0.03. Note that the three stars with the greatest discrepancy in angular size are \( \xi \) Per, \( \xi \) Ori A, and \( \xi \) Oph. However, the results for the first two of these, \( \xi \) Per and \( \xi \)
Ori A, are preliminary because the diameters are based upon one data bracket. ζ Oph is rotationally distorted, so gravity darkening will complicate the meaning of θ LD and the comparison to a model-predicted size may not be entirely valid. The targets with many observations, λ Ori A and 10 Lac, show good agreement between the interferometric and spectroscopically derived angular diameters.

We can use the angular size and distance to obtain the stellar radius. In Table 9 we list distance estimates from the six sources. The columns labeled $d_1$ and $d_2$ give distances based upon a calibration of absolute magnitude and spectral classification from Shull & van Steenberg (1985) and Underhill et al. (1979), respectively. The next estimate $d_3$ is based upon the interstellar Ca II line strengths (Megier et al. 2009).
fourth estimate $d_4$ is derived from the *Hipparcos* parallax (van Leeuwen 2007) with a correction term for the Lutz–Kelker bias (Maíz Apellániz et al. 2008). The next estimate $d_5$ is the distance to the host cluster (Kharchenko et al. 2005) or association (de Zeeuw et al. 1999) if the target is a known member. The final value $d_6$ is derived from the parallaxes from *Gaia* DR2 (Gaia Collaboration et al. 2018). The DR2 coverage is incomplete for bright stars (no measurements for $\xi$ Per and $\zeta$ Ori A) and the errors are relatively large and probably underestimated (Luri et al. 2018). Consequently, we adopted the parallax of fainter, physical companions whenever possible. The DR2 parallaxes for $\lambda$ Ori A, B have large errors, so we adopted the mean of the parallaxes for components C and D. There is no parallax given for $\zeta$ Ori A, so we used the listing for the C component. We applied the parallax of component B for 10 Lac, because of the much larger error associated with component A. There was no faint companion available to use for $\alpha$ Cam, so the formal *Gaia* DR2 parallax error is large. Columns 7 and 9 give the stellar radius corresponding to the *Gaia* and mean distance, respectively, as derived from our

![Figure 4](image-url)
Our interferometric survey of O-star diameters yields results that are comparable to the expected diameters based upon the published temperatures and model fits of the SED (Table 6; Figure 5), except in the cases of two evolved stars, ξ Per and ζ Ori A, where our data coverage is quite limited. Additional interferometric observations are needed to confirm the smaller and larger diameters found in these two cases, respectively. There are several possible explanations for such discrepancies. First, it is possible that some of our calibrator stars have yet undetected binary companions. If such companions added angular size measurements (Table 6). Note that the standard deviation of the mean distance may underestimate the total uncertainty if some subsets rely upon the same spectroscopic calibration of spectral type and $M_V$. The radius range listed for ζ Oph (HD 149757) relates to the smaller and larger angular sizes found at different position angles. The derived radii generally agree within the range associated with their spectral classifications as given by Martins et al. (2005), except for the two giants, ξ Per and ζ Ori A, which have radii closer to those of main sequence stars.

Figure 5. Observed angular size $\theta_D$ compared to $\theta_{LD}(T_{\text{eff}})$ derived from the published $T_{\text{eff}}$ and fit to the SED. The solid line shows a line with a slope of unity for reference, and the dashed line shows the trend for the mean ratio of these diameters. Blue points indicate diameter estimates based upon only a single data bracket or an extremely small angular size in the case of 10 Lac.

incoherent flux to the visibility measurements, then the calibrator visibilities would be depressed and we would infer smaller diameters for the targets. Additional observations with different calibrators would test this idea. Second, it is possible that the quoted diameters of the calibrators have larger than expected uncertainties. The JSDC diameter estimates (Chelli et al. 2016) rely on relations based upon colors and spectral classification that are set by measured angular sizes. However, there are relatively few measurements among the B-type and early A-type stars that form our set of calibrators (Table 4), so the relations may need more thorough testing.

Finally, it is possible that the model atmospheres that we used to fit the SEDs underestimate or overestimate the flux over the observed range (1200 Å to 2 μm), so that the angular diameters inferred from the SED fits are too large or small. All our fits rely on the TLUSTY grid of models (Lanz & Hubeny 2003) which assume a plane-parallel geometry and neglect stellar winds. We made a spot check of the models against the predictions of the non-LTE code CMFGEN (Hillier & Miller 1998) that can account for this.
for spherical geometry and outflows. The initial comparison was made assuming $T_{\text{eff}} = 34.4$ kK, $\log g = 3.5$, solar abundances, and a microturbulent velocity of 10 km s$^{-1}$. A comparison of the predicted fluxes between a plane-parallel model from CMFGEN and one from TLUSTY showed better than 1% agreement in flux ratio over the observed range. This confirms earlier results showing excellent agreement between TLUSTY and CMFGEN (Hillier & Lanz 2001). Additional tests indicated that the mean flux over the observed range was about 1% higher in a CMFGEN spherical model with wind loss and was about 2% higher in models with the microturbulent velocity increased to 20 km s$^{-1}$. Thus, while model differences may account for angular size discrepancies of a few percent, the larger difference seen in the supergiant $\zeta$ Ori A may require other explanations. Interferometric observations at longer wavelengths would help test models that include winds, because of the increasing proportion of wind flux into the IR regime. We will extend this investigation in a subsequent paper to the cooler B-type stars to further explore the differences between interferometrically and spectroscopically determined parameters for massive stars.

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Software: TLUSTY (Hubeny & Lanz 1995; Lanz & Hubeny 2003, 2007), CMFGEN (Hubill & Miller 1998).

### ORCID iDs

Kathryn D. Gordon @ https://orcid.org/0000-0003-1338-531X
Douglas R. Gies @ https://orcid.org/0000-0001-8537-3583
Gail H. Schaefer @ https://orcid.org/0000-0001-5415-9189
Daniel Huber @ https://orcid.org/0000-0001-8832-4488
Michael Ireland @ https://orcid.org/0000-0002-6194-043X

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