Extraposition Grammars

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Extraposition grammars are an extension of definite clause grammars, and are similarly defined in terms of logic clauses. The extended formalism makes it easy to describe left extraposition of constituents, an important feature of natural language syntax.

1. Introduction

This paper presents a grammar formalism for natural language analysis, called extraposition grammars (XGs), based on the subset of predicate calculus known as definite, or Horn, clauses. It is argued that certain important linguistic phenomena, collectively known in transformational grammar as left extraposition, can be described better in XGs than in earlier grammar formalisms based on definite clauses.

The XG formalism is an extension of the definite clause grammar (DCG) [6] formalism, which is itself a restriction of Colmerauer’s formalism of metamorphosis grammars (MGs) [2]. Thus XGs and MGs may be seen as two alternative extensions of the same basic formalism, DCGs.

The argument for XGs will start with a comparison with DCGs. I should point out, however, that the motivation for the development of XGs came from studying large MGs for natural language [4,7].

The relationship between MGs and DCGs is analogous to that between type-0 grammars and context-free grammars. So, some of the linguistic phenomena which are seen as rewriting one sequence of constituents into another might be described better in a MG than in a DCG. However, it will be shown that rewritings such as the one involved in left extraposition cannot easily be described in either of the two formalisms.

Left extraposition has been used by grammarians to describe the form of interrogative sentences and relative clauses, at least in languages such as English, French, Spanish and Portuguese. The importance of these constructions, even in simplified subsets of natural language, such as those used in database interfaces, suggests that a grammar formalism should be able to express them in a clear and concise manner. This is the purpose of XGs.

2. Grammars in Logic

This section summarises the concepts of definite clause grammars (DCGs), and of the underlying system of logic, definite clauses, needed for the rest of the paper. A fuller discussion can be found elsewhere [6].

A definite clause has either the form

\[ P \leftarrow Q_1, \ldots, Q_n \]

to be read as “P is true if \( Q_1, \ldots, Q_n \) are true”, or the form

\[ P \]

to be read as “P is true”. \( P \) is the head of the clause, \( Q_1, \ldots, Q_n \) are goals, forming the body of the clause. The symbols \( P, Q_1, \ldots, Q_n \) stand for literals. A literal has a predicate symbol, and possibly some arguments (in parentheses, separated by commas), e.g.

\[ \text{father}(X,Y) \quad \text{false} \quad \text{number}(0) \]

A literal is to be interpreted as denoting a relation between its arguments; e.g. “father(X,Y)” denotes the relation ‘father’ between X and Y.

Arguments are terms, standing for partially specified objects. Terms may be

• variables, denoting unspecified objects (variable names are capitalised):
  \( X \)  Case Agreement

• atomic symbols, denoting specific objects:
  \( \text{plural}[3] \)

• compound terms, denoting complex objects:
  \( s(NP,VP) \quad \text{succ(succ}(0)) \)

A compound term has a functor and some arguments, which are terms. Compound terms are best seen as

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A particular type of term, the *list*, has a simplified notation. The binary functor '+' makes up non-empty lists, and the atom '[' ']' denotes the empty list. In the special list notation,

\[ [a,b] \text{ [X I Y]} \]

represent respectively the terms

\[ .(a,.(b,[])) .(X,Y) \]

Putting these concepts together, the clause

\[ \text{grandfather}(X,Z) :- \text{father}(X,Y), \text{parent}(Y,Z). \]

may be read as "X is grandfather of Z if X is father of Y and Y is a parent of Z"; the clause

\[ \text{father}(\text{john}, \text{mary}). \]

may be read as "John is father of Mary" (note the use of lower case for the constants in the clause).

A set of definite clauses forms a *program*. A program defines the relations denoted by the predicates appearing on the head of clauses. When using a definite clause interpreter, such as PROLOG [9], a *goal statement*

? - P.

specifies that the relation instances that match P are required.

Now, any context-free rule, such as

\[ \text{sentence} \rightarrow \text{noun phrase}, \text{verb phrase}. \]

(I use ' ; ' for concatenation, and ' . ' to terminate a rule) may be translated into a definite clause

\[ \text{sentence}(S0,S) :- \text{noun phrase}(S0,S1), \text{verb phrase}(S1,S). \]

which says: "there is a sentence between points S0 and S in a string if there is a noun phrase between points S0 and S1, and a verb phrase between points S1 and S". A context-free rule like

\[ \text{determiner} \rightarrow [\text{the}]. \]

(where the square brackets mark a terminal) can be translated into

\[ \text{determiner}(S0,S) :- \text{connects}(S0,\text{the},S). \]

which may be read as "there is a determiner between points S0 and S in a string if S0 is joined to S by the word 'the'". The predicate 'connects' is used to relate terms denoting points in a string to the words which join those points. Depending on the application, different definitions of 'connects' might be used. In particular, if a point in a string is represented by the list of words after that point, 'connects' has the very simple definition

\[ \text{connects}([\text{Word][S]],\text{Word},S). \]

DCGs are the natural extension of context-free grammars (CFGs) obtained through the translation into definite clauses outlined above. A DCG non-terminal may have arguments, of the same form as those of a predicate, and a terminal may be any term. For instance, the rule

\[ \text{sentence}(s(NP,VP)) :- \text{noun phrase}(NP,N), \text{verb phrase}(VP,N). \]

states: "A sentence with structure

\[ s \]

\[ / \]

\[ \text{NP} \text{ VP} \]

is made of a noun phrase with structure NP and number N (which can be either 'singular' or 'plural'), followed by a verb phrase with structure VP agreeing with the number N". A DCG rule is just "syntactic sugar" for a definite clause. The clause for the example above is

\[ \text{sentence}(s(NP,VP),S0,S) :- \text{noun phrase}(NP,N,S0,S1), \text{verb phrase}(VP,N,S1,S). \]

In general, a DCG non-terminal with n arguments is translated into a predicate of n+2 arguments, the last two of which are the string points, as in the translation of context-free rules into definite clauses.

The main idea of DCGs is then that grammar symbols can be *general logic terms* rather than just atomic symbols. This makes DCGs a general-purpose grammar formalism, capable of describing any type-0 language. The first grammar formalism with logic terms as grammar symbols was Colmerauer's metamorphosis grammars [2]. Where a DCG is a CFG with logic terms for grammar symbols, a MG is a somewhat restricted type-0 grammar with logic terms for grammar symbols. However, the very simple translation of DCGs into definite clauses presented above does not carry over directly to MGs.

3. Left Extraposition

Roughly speaking, *left extraposition* occurs in a natural language sentence when a subconstituent of some constituent is missing, and some other constituent, to the left of the incomplete one, represents the missing constituent in some way. It is useful to think that an empty constituent, the *trace*, occupies the "hole" left by the missing constituent, and that the constituent to the left, which represents the missing part, is a *marker*, indicating that a constituent to its right contains a trace [1]. One can then say that the constituent in whose place the trace stands has been extraposed to the left, and, in its new position, is rep-
sentence --> noun_phrase, verb_phrase.
noun_phrase --> proper_noun.
noun_phrase --> determiner, noun, relative.
noun_phrase --> determiner, noun, prep_phrase.
noun_phrase --> trace.  \[\text{(1)}\]
trace --> [ ].
verb_phrase --> verb, noun_phrase.
verb_phrase --> verb.
relative --> [ ].
relative --> rel_pronoun, sentence.
prep_phrase --> preposition, noun_phrase.

Figure 4.1. CFG for relative clauses.

represented by the marker. For instance, relative clauses
are formed by a marker, which in the simpler cases is just a relative
pronoun, followed by a sentence where some noun phrase has been replaced by a trace. This
is represented in the following annotated surface struc-
ture:
The man that/ [sdohn met \[t i\] is a grammarian.

In this example, \[t\] stands for the trace, ‘that’ is the
surface form of the marker, and the connection be-
tween the two is indicated by the common index \[i\].

The concept of left extraposition plays an essential
role, directly or indirectly, in many formal descriptions
of relative and interrogative clauses. Related to this
concept, there are several “global constraints”, the
“island constraints”, that have been introduced to
restrict the situations in which left extraposition can
be applied. For instance, the Ross complex-NP con-
straint \[8\], implies that any relative pronoun occurring
outside a given noun phrase cannot be bound to a
trace occurring inside a relative clause which is a sub-
constituent of the noun phrase. This means that it is
not possible to have a configuration like

\[X_1 \ldots [\text{np} \ldots [\text{rel} \quad x_2 \quad [s \ldots t_2 \ldots t_1 \ldots ] \ldots ] \ldots ]\]

Note that here I use the concept of left extraposi-
tion in a loose sense, without relating it to transfor-
mations as in transformational grammar. In XGs, and also
in other formalisms for describing languages (for in-
stance the context-free rule schemas of Gazdar \[5\]),
the notion of transformation is not used, but a concep-
tual operation of some kind is required for instance to
relate a relative pronoun to a “hole” in the structural
representation of the constituent following the pro-
noun.

4. Limitations of Other Formalisms

To describe a fragment of language where left ex-
traposition occurs, one might start with a CFG which
gives a rough approximation of the fragment. The
grammar may then be refined by adding arguments to
non-terminals, to carry extraposed constituents across
phrases. This method is analogous to the introduction
of “derived” rules by Gazdar \[5\]. Take for example
the CFG in Figure 4.1. In this grammar it is possible
to use rule (1) to expand a noun phrase into a trace,
even outside a relative clause. To prevent this, I will
add arguments to all non-terminals from which a noun
phrase might be extraposed. The modified grammar,
now a DCG, is given in Figure 4.2. A variable
\[\text{‘Hole...’}\] will have the value ‘trace’ if an extraposed
noun phrase occurs somewhere to the right, ‘nil’ other-
wise. The parse tree of Figure 4.3 shows the variable
values when the grammar of Figure 4.2 is used to ana-
lyse the noun phrase “the man that John met”.

Intuitively, we either can see noun phrases moving
to the left, leaving traces behind, or traces appearing
from markers and moving to the right. In a phrase
“\text{noun_phrase(Hole1,Hole2)}”, Hole1 will have the
value ‘trace’ when a trace occurs somewhere to the
right of the left end of the phrase. In that case, Hole2
will be ‘nil’ if the noun phrase contains the trace,
‘trace’ if the trace appears to the right of the right end
of this noun phrase. Thus, rule (2) in Figure 4.2 speci-
fies that a noun phrase expands into a trace if a trace
appears from the left, and as this trace is now placed,
will not be found further to the right.

The non-terminal ‘relative’ has no arguments, be-
cause the complex-NP constraint prevents noun phras-
es from moving out of a relative clause. However, that
constraint does not apply to prepositional phrases, so
‘\text{prep_phrase}’ has arguments. The non-terminal
‘sentence’ (and consequently ‘verb_phrase’) has a
single argument, because in a relative clause the trace
must occur in the sentence immediately to the right of the relative pronoun.

It is obvious that in a more extensive grammar, many non-terminals would need extraposition arguments, and the increased complication would make the grammar larger and less readable.

Colmerauer’s MG formalism allows an alternative way to express left extraposition. It involves the use of rules whose left-hand side is a non-terminal followed by a string of “dummy” terminal symbols which do not occur in the input vocabulary. An example of such a rule is:

rel_marker, [t] --> rel_pronoun.

Its meaning is that ‘rel_pronoun’ can be analysed as a ‘rel_marker’ provided that the terminal ‘t’ is added to the front of the input remaining after the rule application. Subsequent rule applications will have to cope explicitly with such dummy terminals. This method has been used in several published grammars [2, 4, 7], but in a large grammar it has the same (if not worse) problems of size and clarity as the previous method. It also suffers from a theoretical problem: in general, the language defined by such a grammar will contain extra sentences involving the dummy terminals. For parsing, however, no problem arises, because the input sentences are not supposed to contain dummy terminals. These inadequacies of MGs were the main motivation for the development of XGs.

5. Informal Description of XGs

To describe left extraposition, we need to relate non-contiguous parts of a sentence. But neither DCGs nor MGs have means of representing such a relationship by specific grammar rules. Rather, the relationship can only be described implicitly, by adding extra information to many unrelated rules in the grammar. That is, one cannot look at a grammar and find a set of rules specific to the constructions which involve left extraposition.

With extraposition grammars, I attempt to provide a formalism in which such rules can be written.

In this informal introduction to the XG formalism, I will avoid the extra complications of non-terminal arguments. So, in the discussion that follows, we may look at XGs as an extension of CFGs.

Sometimes it is easier to look at grammar rules in the left-to-right, or synthesis, direction. I will say then that a rule is being used to expand or rewrite a string. In other cases, it is easier to look at a rule in the right-to-left, or analysis, direction. I will say then that the rule is being used to analyse a string.

Let us first look at the following XG fragment:

sentence --> noun_phrase, verb_phrase.
noun_phrase --> determiner, noun, relative, noun_phrase --> trace.
relative --> [ ].
relative --> rel_marker, sentence.
rel_marker ... trace --> rel_pronoun.
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the mouse rel_marker the cat chased trace squeaks

the mouse rel_pronoun the cat chased squeaks

Figure 5.1. Applying an XG rule.

All rules but the last are context-free. The last rule expresses the extraposition in simple relative clauses. It states that a relative pronoun is to be analysed as a marker, followed by some unknown constituents (denoted by '...'), followed by a trace. This is shown in Figure 5.1. As in the DCG example of the previous section, the extraposed noun phrase is expanded into a trace. However, instead of the trace being rewritten into the empty string, the trace is used as part of the analysis of 'rel_marker'.

The difference between XG rules and DCG rules is then that the left-hand side of an XG rule may contain several symbols. Where a DCG rule is seen as expressing the expansion of a single non-terminal into a string, an XG rule is seen as expanding together several non-contiguous symbols into a string. More precisely, an XG rule has the general form

\[ s_1 \ldots s_2 \text{ etc. } s_{k-1} \ldots s_k \rightarrow r. \]  (3)

Here each segment \( s_i \) (separated from other segments by '...') is a sequence of terminals and non-terminals (written in DCG notation, with ',' for concatenation). The first symbol in \( s_1 \), the leading symbol, is restricted to be a non-terminal. The right-hand side \( r \) is as in a DCG rule.

Leaving aside the constraints discussed in the next section, the meaning of a rule like (3) is that any sequence of symbols of the form

\[ s_1x_1s_2x_2 \text{ etc. } s_{k-1}x_{k-1}s_k \]

with arbitrary \( x_i \)'s, can be rewritten into \( rx_1x_2\ldots x_{k-1} \).

Thinking procedurally, one can say that a non-terminal may be expanded by matching it to the leading symbol on the left-hand side of a rule, and the rest of the left-hand side is "put aside" to wait for the derivation of symbols which match each of its symbols in sequence. This sequence of symbols can be interrupted by arbitrary strings, paired to the occurrences of '...' on the left-hand side of the rule.

6. XG Derivations

When several XG rules are involved, the derivation of a surface string becomes more complicated than in the single rule example of the previous section, because rule applications interact in the way now to be described.

To represent the intermediate stages in an XG derivation, I will use bracketed strings, made up of
- terminal symbols
- non-terminal symbols
- the open bracket <
- the close bracket >

A bracketed string is balanced if the brackets in it balance in the usual way.

Now, an XG rule

\[ u_1 \ldots u_2 \ldots \text{ etc. } \ldots u_n \rightarrow v, \]

can be applied to bracketed string \( s \) if

\[ s = x_0u_1x_1u_2 \text{ etc. } x_{n-1}u_nx_n \]

and each of the gaps \( x_1, \ldots, x_{n-1} \) is balanced. The substring of \( s \) between \( x_0 \) and \( x_n \) is the span of the rule application. The application rewrites \( s \) into new string \( t \), replacing \( u_1 \) by \( v \) followed by \( n-1 \) open brackets, and replacing each of \( u_2, \ldots, u_n \) by a close bracket; in short, \( s \) is replaced by

\[ x_0v< \ldots <x_1>x_2> \ldots x_{n-1}>x_n \]

The relation between the original string \( s \) and the derived string \( t \) is abbreviated as \( s \Rightarrow t \). In the new string \( t \), the substring between \( x_0 \) and \( x_n \) is the result of the application. In particular, the application of a rule with a single segment in its left-hand side is no different from what it would be in a type-0 grammar.

Taking again the rule

\[ \text{rel_marker } \ldots \text{ trace } \rightarrow \text{ rel_pronoun.} \]

its application to

\[ \text{rel_marker John likes trace} \]

produces

\[ \text{rel_pronoun < John likes >} \]

After this rule application, it is not possible to apply any rule with a segment matching inside a bracketed portion and another segment matching outside it. The use of the above rule has divided the string into two isolated portions, each of which must be independently expanded.

Given an XG with initial symbol \( s \), a sentence \( t \) is in the language defined by the XG if there is a se-
Figure 7.1. Derivation graph for "aabbcc".

If one follows to the letter the definitions in this section, then checking, in a parsing procedure, whether an XG rule may be applied, would require a scan of the whole intermediate string. However, we will see in Section 10 that this check may be done "on the fly" as brackets are introduced, with a cost independent of the length of the current intermediate string in the derivation.

7. Derivation Graphs

In the same way as parse trees are used to visualise context-free derivations, I use derivation graphs to represent XG derivations.

In a derivation graph, as in a parse tree, each node corresponds to a rule application or to a terminal symbol in the derived sentence, and the edges leaving a node correspond to the symbols in the right-hand side of that node's rule. In a derivation graph, however, a node can have more than one incoming edge - in fact, one such edge for each of the symbols on the left-
hand side of the rule corresponding to that node. Of these edges, only the one corresponding to the leading symbol is used to define the left-to-right order of the symbols in the sentence whose derivation is represented by the graph. If one deletes from a derivation graph all except the first of the incoming edges to every node, the result is a tree analogous to a parse tree.

For example, Figure 7.1 shows the derivation graph for the string "aabbcc" according to the XG:

\[
\begin{align*}
S & \rightarrow as, bs, cs. \\
as & \rightarrow [\ ]. \\
as \ldots xb & \rightarrow [a], as. \\
bs & \rightarrow [\ ]. \\
bs \ldots xc & \rightarrow xb, [b], bs. \\
cs & \rightarrow [\ ]. \\
cs & \rightarrow xc, [c], cs.
\end{align*}
\]

This XG defines the language formed by the set of all strings

\[a^n b^n c^n \text{ for } n \geq 0.\]

The example shows, incidentally, that XGs, even without arguments, are strictly more powerful than CFGs, since the language described is not context-free.

The topology of derivation graphs reflects clearly the bracketing constraint. Assume the following two conventions for the drawing of a derivation graph, which are followed in all the graphs shown here:

- the edges entering a node are ordered clockwise following the sequence of the corresponding symbols in the left-hand side of the rule for that node;
- the edges issuing from a node are ordered counterclockwise following the sequence of the corresponding symbols in the right-hand side of the rule for the node.

Then the derivation graph obeys the bracketing constraint if and only if it can be drawn, following the conventions, without any edges crossing. The example of Figure 7.2 shows this clearly. In this figure, the closed path formed by edges 1, 2, 3, and 4 has the same effect as a matching pair of brackets in a bracketed string.

It is also worth noting that nested rule applications appear in a derivation graph as a configuration like the one depicted in Figure 7.3.

8. XGs and Left Extraposition

We saw in Figure 4.2 a DCG for (some) relative clauses. The XG of Figure 8.1 describes essentially the same language fragment, showing how easy it is to describe left extraposition in an XG. In that grammar, the sentence

\[
\text{The mouse that the cat chased squeaks.}
\]

has the derivation graph shown in Figure 8.2. The left extraposition implicit in the structure of the sentence is represented in the derivation graph by the applica-

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1 In some of the examples of this article, edges cross to make the graphs more readable, but such crossings could be trivially avoided.
Figure 8.2. Example of derivation graph for the XG in Figure 8.1.

In the rest of this paper, I often refer to a constituent being repositioned into a bracketed string (or into a fragment of derivation graph), to mean that a rule having that constituent as a non-leading symbol in the left-hand side has been applied, and the symbol matches some symbol in the string (or corresponds to some edge in the fragment). For example, in Figure 8.2 the trace ‘t’ is repositioned into the subgraph with root ‘s’.

9. Using the Bracketing Constraint

In the example of Figure 8.2, there is only one application of a non-DCG rule, at the place marked (*). However, we have seen that when a derivation contains several applications of such rules, the applications must obey the bracketing constraint. The use of the constraint in a grammar is better explained with an example. From the sentences

- The mouse squeaks.
- The cat likes fish.
- The cat chased the mouse.

Figure 8.1. XG for relative clauses.

Figure 8.2. Example of derivation graph for the XG in Figure 8.1.
the grammar of Figure 8.1 can derive the following string, which violates the complex-NP constraint:

* The mouse that the cat that chased likes fish squeaks.

The derivation of this ungrammatical string can be better understood if we compare it with a sentence outside the fragment:

The mouse, that the cat which chased it likes fish, squeaks.

where the pronoun ‘it’ takes the place of the incorrect trace.

The derivation graph for that un-English string is shown in Figure 9.1. In the graph, (*) and (**) mark two nested applications of the rule for ‘rel__marker’. The string is un-English because the higher ‘relative’ (marked (+) in the graph) binds a trace occurring inside a sentence which is part of the subordinated ‘noun_phrase’ (+ +).

Now, using the bracketing constraint one can neatly express the complex-NP constraint. It is only necessary to change the second rule for ‘relative’ in Figure 8.1 to

relative → open, rel_marker, sentence, close. (5)

and add the rule

open ... close → [ ] . (6)

With this modified grammar, it is no longer possible to violate the complex-NP constraint, because no constituent can be repositioned from outside into the gap created by the application of rule (6) to the result of applying the rule for relatives (5).

The non-terminals ‘open’ and ‘close’ bracket a subderivation

... open x close ... → < x > ...

preventing any constituent from being repositioned from outside that subderivation into it. Figure 9.2 shows the use of rule (6) in the derivation of the sentence

The mouse that the cat that likes fish chased squeaks.

This is based on the same three simple sentences as the ungrammatical string of Figure 9.1, which the
Like a DCG, a general XG is no more than a convenient notation for a set of definite clauses. An XG non-terminal of arity $n$ corresponds to an $n+4$ place predicate (with the same name). Of the extra four arguments, two are used to represent string positions as in DCGs, and the other two are used to represent positions in an extraposition list, which carries symbols to be repositioned.

Each element of the extraposition list represents a symbol being repositioned as a 4-tuple

$$x(\text{context}, \text{type}, \text{symbol}, xlist)$$

where context is either 'gap', if the symbol was preceded by '...', in the rule where it originated, or 'nogap', if the symbol was preceded by ';'; type may be 'terminal' or 'nonterminal', with the obvious meaning; symbol is the symbol proper; xlist is the remainder of the extraposition list (an empty list being represented by '[' ']').
An XG rule is translated into a clause for the predicate corresponding to the leading symbol of the rule. In the case where the XG rule has just a single symbol on the left-hand side, the translation is very similar to that of DCG rules. For example, the rule

```plaintext
sentence --> noun_phrase, verb_phrase.
```

translates into

```plaintext
sentence(S0,S,X0,X) :-
  noun_phrase(S0,S1,X0,X1),
  verb_phrase(S1,S,X1,X).
```

A terminal t in the right-hand side of a rule translates into a call to the predicate 'terminal', defined below, whose role is analogous to that of 'connects' in DCGs. For example, the rule

```plaintext
rel_pronoun --> [that].
```

translates into

```plaintext
rel_pronoun(S0,S,X0,X) :-
  terminal(that,S0,S,X0,X).
```

The translation of a rule with more than one symbol in the left-hand side is a bit more complicated. Informally, each symbol after the first is made into a 4-tuple as described above, and fronted to the extraposition list. Thus, for example, the rule

```plaintext
rel_marker ... trace --> rel_pronoun.
```

translates into

```plaintext
rel_marker(S0,S,X0,X) :-
  rel_pronoun(S0,S,X0,X).
```

Furthermore, for each distinct non-leading non-terminal nt (with arity n) in the left-hand side of a rule of the XG, the translation includes the clause

```plaintext
nt(V1,...,Vn,S,S,X0,X) :-
  virtual(nt(V1,...,Vn),S,S,X0,X).
```

where 'virtual(C,X0,X)', defined later, can be read as "C is the constituent between X0 and X in the extraposition list", and the variables Vi transfer the arguments of the symbol in the extraposition list to the predicate which translates that symbol.

For example, the rule

```plaintext
marker(Var), [the] ... [of.whom], trace(Var) --> [whose].
```

which can be used in a more complex grammar of relative clauses to transform "whose X" into "the X of whom", corresponds to the clauses:

```plaintext
marker(Var,S0,S,X0),
  x(nogap,terminal,the, x(gap,terminal,of, x(nogap,terminal,whom, x(nogap,nonterminal,trace(Var), X ))) :-
  terminal(whose,S0,S,X0,X).

trace(Var,S,S,X0,X) :- virtual(trace(Var),X0,X).
```

Finally, the two auxiliary predicates 'virtual' and 'terminal' are defined as follows:

```plaintext
virtual(NT, x(C,nonterminal,NT,X), X).
terminal(T, S0, S, X, X) :-
  gap(X), connects(S0, T, S).
terminal(T, S, x(C,terminal,T,X), X).

gap(x(gap,T,S,X)).
```

where 'connects' is as for DCGs.

These definitions need some comment. The first clause for 'terminal' says that, provided the current extraposition list allows a gap to appear in the derivation, terminal symbol T may be taken from the position S0 in the source string, where T connects S0 to some new position S. The second clause for 'terminal' says that if the next symbol in the current extraposition list is a terminal T, then this symbol can be taken as if it occurred at S in the source string. The clause for 'virtual' allows a non-terminal to be "read off from" the extraposition list.

```
* relative(6,9,X,X)
* open(6,6,x(gap,nt,trace,x(gap,nt,close,[])), x(gap,nt,close,x(gap,nt,trace, x(gap,nt,close,[]))))
* rel_marker(6,7,x(gap,nt,close,x(gap,nt,trace, x(gap,nt,close,[]))), x(gap,nt,trace,x(gap,nt,close,[]))))
* rel_pronoun(6,7,X,X)
  [that]
* sentence(7,9,x(gap,nt,trace,x(gap,nt,close, x(gap,nt,trace,x(gap,nt,close,[])))), x(gap,nt,trace,x(gap,nt,close,[]))))
* noun_phrase(7,7,x(gap,nt,trace,x(gap,nt,close, x(gap,nt,trace,x(gap,nt,close,[])))), x(gap,nt,trace,x(gap,nt,close,[]))))
* verb_phrase(7,9,X,X)
* verb(7,8,X,X)
  [likes]
* noun_phrase(8,9,X,X)
* determiner(8,8,X,X)
* noun(8,9,X,X)
  [fish]
* relative(9,9,X,X)
* close(9,9,x(gap,nt,close,x(gap,nt,trace, x(gap,nt,close,[]))), x(gap,nt,trace,x(gap,nt,close,[]))))
```

Figure 10.1. Derivation of “that likes fish”.

Figure 10.1 shows a fragment of the analysis in Figure 9.2, but now in terms of the translation of XG rules into definite clauses. Points on the sentence are labelled as follows:
The nodes of the analysis fragment, for the relative clause "that likes fish", are represented by the corresponding goals, indented in proportion to their distance from the root of the graph. The following conventions are used to simplify the figure:

- The leaves (terminals) of the graph are listed directly;
- the values of the extraposition arguments are explicitly represented only for those goals that add or delete something to the extraposition list; for the other goals, the two identical values are represented by the variable 'X';
- the goals for 'terminal' and 'virtual' are left out as they can be easily reconstructed from the other goals and the definitions above;
- 'nonterminal' is abbreviated as 'nt'.

The definite clause program corresponding to the grammar for this example is listed in Appendix II.

The example shows clearly how the bracketing constraint works. Symbols are placed in the extraposition list by rules with more than one symbol in the left-hand side, and removed by calls to 'virtual', on a first-in-last-out basis; that is, the extraposition list is a stack. But this property of the extraposition list is exactly what is needed to balance "on the fly" the auxiliary brackets in the intermediate steps of a derivation.

Being no more than a logic program, an XG can be used for analysis and for synthesis in the same way as a DCG. For instance, to determine whether a string \( s \) with initial point \( \text{initial} \) and final point \( \text{final} \) is in the language defined by the XG of Figure 8.1, one tries to prove the goal statement

\[ ?- \text{sentence}(	ext{initial},	ext{final},[ 
\],
\] [ ]).

As for DCGs, the string \( s \) can be represented in several ways. If it is represented as a list, the above goal would be written

\[ ?- \text{sentence}(s,[ 
\],
\] [ ],
\] [ ]).

The last two arguments of the goal are \([ \ ]\) to mean that the overall extraposition list goes from \([ \ ]\) to \([ \ ]\); i.e., it is the empty list. Thus, no constituent can be repositioned into or out of the top level 'sentence'.

11. Conclusions and Further Work

In this paper I have proposed an extension of DCGs. The motivation for this extension was to provide a simple formal device to describe the structure of such important natural language constructions as relative clauses and interrogative sentences. In transformational grammar, these constructions have usually been analysed in terms of left extraposition, together with global constraints, such as the complex-NP constraint, which restrict the range of the extraposition. Global constraints are not explicit in the grammar rules, but are given externally to be enforced across rule applications. These external global constraints cause theoretical difficulties, because the formal properties of the resulting systems are far from evident, and practical difficulties, because they lead to obscure grammars and prevent the use of any reasonable parsing algorithm.

DCGs, although they provide the basic machinery for a clear description of languages and their structures, lack a mechanism to describe simply left extraposition and the associated restrictions. MGs can express the rewrite of several symbols in a single rule, but the symbols must be contiguous, as in a type-0 grammar rule. This is still not enough to describe left extraposition without complicating the rest of the grammar. XGs are an answer to those limitations.

An XG has the same fundamental property as a DCG, that it is no more than a convenient notation for the clauses of an ordinary logic program. XGs and their translation into definite clauses have been designed to meet three requirements: (i) to be a principled extension of DCGs, which can be interpreted as a grammar formalism independently of its translation into definite clauses; (ii) to provide for simple description of left extraposition and related restrictions; (iii) to be comparable in efficiency with DCGs when executed by PROLOG. It turns out that these requirements are not contradictory, and that the resulting design is extremely simple. The restrictions on extraposition are naturally expressed in terms of scope, and scope is expressed in the formalism by "bracketing out" subderivations corresponding to balanced strings. The notion of bracketed string derivation is introduced in order to describe extraposition and bracketing independently of the translation of XGs into logic programs.

Some questions about XGs have not been tackled in this paper. First, from a theoretical point of view it would be necessary to complete the independent characterisation of XGs in terms of bracketed strings, and show rigorously that the translation of XGs into logic programs correctly renders this independent characterisation of the semantics of XGs. As pointed out before, this formalisation does not offer any substantial problems.

Next, it is not clear whether XGs are as general as they could be. For instance, it might be possible to extend them to handle right extraposition of constituents, which, although less common than left extraposition, can be used to describe quite frequent English constructions, such as the gap between head noun and relative clause in:

\[ \text{What files are there that were created today?} \]
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It may however be possible to describe such situations in terms of left extrapolation of some other constituent (e.g. the verb phrase “are there” in the example above).

Finally, I have been looking at what transformations should be applied to an XG developed as a clear description of a language, so that the resulting grammar could be used more efficiently in parsing. In particular, I have been trying to generalise results on deterministic parsing of context-free languages into appropriate principles of transformation.

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Appendix I. Translating XGs

The following PROLOG program (for the DEC-10 PROLOG system) defines a predicate ‘grammar(File)’ which translates and stores the XG rules contained in File. The symbol ‘_’ as a predicate or functor argument denotes an “anonymous” variable, i.e. each such occurrence stands for a separate variable with a single occurrence.

% Definition of the grammar rule operators
:- op(1001,xfy, (...)).
:- op(1200,xfx,(=

% Process the XG in File
grammar(File) :-
seeing(Old),
see(File),
consume,
seen,
see(Old).
% Loop until end_of_file
consume :-
repeat,
read(X),
( X=end_of_file, !;
process(X),
fail).
% Process a grammar rule
process((L=\rightarrow R)) :- !,
expandlhs(T,SO,S,HO,HI,Q),
expandrhs(R,SO,S,HO,H,Q),
assertz((P :- Q)), !.
% Execute a command
process(( :- G)) :- !,
G.
% Store a normal clause
process((P :- Q)) :-
assertz((P :- Q)).
% Store a unit clause
process(P) :-
assertz(P).
% Translate an XG rule
% Translate the left-hand side
expandlhs(T,SO,S,HO,HI,Q) :-
flatten(T,[P | L1],[]),
front(L,HI,H),
tag(P,SO,S,HO,H,Q).
flatten((X...Y),L0,L) :- !,
flatten(X,L0,[gap | L1]),
flatten(Y,L1,L).
flatten((X,Y),L0,L) :- !,
flatten(X,L0,[nogap | L1]),
flatten(Y,L1,L).
flatten(X,[X | L1].
front([]),H,H).
front([X | L1],HO,H) :-
case(X,H,terminal,T,H).
unwind(Ts,HO,H).
case(Nt,H,x(K,nonterminal,Nt,H)) :-
virtual_rule(Nt).
% Create the clause
% Nt(S,S,XO,X) :- virtual(Nt,XO,X)
% for extraposed symbol Nt
virtual_rule(Nt) :-
functor(Nt,F,N),
functor(Y,F,N),
tag(Y,S,S,Hx,Hy,P),
( clause(P,virtual(_,_,_),!), !;
asserta((P :- virtual(Y,Hx,Hy))) ).
% Translate the right-hand side
expandrhs((X1,X2),SO,S,HO,H,Y) :- !,
expandrhs(X1,SO,S1,HO,H,Y1),
expandrhs(X2,S1,S,HO,H,Y2),
and(Y1,Y2,Y).
expandrhs((X1;X2),SO,S,HO,H,(Y1;Y2)) :- !,
expandor(X1,SO,S,HO,H,Y1),
expandor(X2,SO,S,HO,H,Y2).
expandrhs([X | L],SO,S,HO,H,X) :-
expandrhs(L,SO,S,HO,H,G) :- istlist(L), !,
expandlist(L,SO,S,HO,H,G).
expandrhs(X,SO,S,HO,H,Y) :-
tag(X,SO,S,HO,H,Y).
expandor(X,SO,S,HO,H,Y) :-
expandor(X,SO,S,HO,H,Ya),
( S\=SOa, !, SO\=SOa, Ya=Yb and(SO=SOa,Ya=Yb) ),
( H\=HOa, !, HO\=HOa, Ya=Yb and(HO=HOa,Yb,Y) ).
expandlist([],S,length(true).
expandlist([X | L],SO,S,HO,H,terminal(X,SO,S,HO,H)) :- !.
expandlist([X | L],SO,S,HO,H).


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\begin{align*}
\text{terminal}(X, SO, SI, HO, H1, Y) & \text{ :- } \text{expandlist}([S1, S, H1, H, Y]). \\
\text{tag}(P, AI, A2, A3, A4, Q) & \text{ :- } \\
& \text{P} = .-[F | \text{Args0}], \\
& \text{conc}(\text{Args0}, [AI, A2, A3, A4], \text{Args}), \\
& \text{Q} = .-[F | \text{Args}]. \\
\text{and}(P, P, P) & \text{ :- } !. \\
\text{and}(P, true, P) & \text{ :- } !. \\
\text{and}(P, Q, P) & \text{ :- } !. \\
\text{islist}([]) & \text{ :- } !. \\
\text{unwind}([], H, H) & \text{ :- } !. \\
\text{unwind}([T | Ts], HO, x(nogap, \text{terminal}, T, H)) & \text{ :- } \\
& \text{unwind}(Ts, HO, H). \\
\text{conc}([], L, L) & \text{ :- } !. \\
\text{conc}([X | L1, L2, [X | L3]]) & \text{ :- } \\
& \text{conc}(L1, L2, L3). \\
\end{align*}

### Appendix II. Definite clauses for the grammar used in Figure 9.2

\begin{align*}
\text{sentence}(SO, S, XO, X) & \text{ :- } \\
& \text{noun_phrase}(SO, S1, XO, X1), \\
& \text{verb_phrase}(S1, S, X1, X). \\
\text{noun_phrase}(SO, S, XO, X) & \text{ :- } \\
& \text{proper_noun}(SO, S, XO, X). \\
\text{noun_phrase}(SO, S, XO, X) & \text{ :- } \\
& \text{determiner}(SO, S1, XO, X1), \\
& \text{noun}(S1, S2, X1, X2), \\
& \text{relative}(S2, S, X2, X). \\
\text{noun_phrase}(SO, S, XO, X) & \text{ :- } \\
& \text{determiner}(SO, S1, XO, X1), \\
& \text{noun}(S1, S2, X1, X2), \\
& \text{prep_phrase}(S2, S, X2, X). \\
\text{noun_phrase}(SO, S, XO, X) & \text{ :- } \\
& \text{trace}(SO, S, XO, X). \\
\text{verb_phrase}(SO, S, XO, X) & \text{ :- } \\
& \text{verb}(SO, S1, XO, X1), \\
& \text{noun_phrase}(S1, S, X1, X). \\
\text{verb_phrase}(SO, S, XO, X) & \text{ :- } \\
& \text{verb}(SO, S, XO, X). \\
\text{relative}(SO, SO, X, X). \\
\text{relative}(SO, S, XO, X) & \text{ :- } \\
& \text{open}(SO, S1, XO, X1), \\
& \text{rel_marker}(S1, S2, X1, X2), \\
& \text{sentence}(S2, S3, X2, X3), \\
& \text{close}(S3, S, X3, X). \\
\text{trace}(SO, SO, XO, X) & \text{ :- } \\
& \text{virtual}(\text{trace}, XO, X). \\
\text{rel_marker}(SO, S, XO, X(gap, nonterminal, trace, X)) & \text{ :- } \\
& \text{rel_pronoun}(SO, S, XO, X). \\
\text{prep_phrase}(SO, S, XO, X) & \text{ :- } \\
& \text{preposition}(SO, S1, XO, X1), \\
& \text{noun_phrase}(S1, S, X1, X). \\
\text{open}(SO, SO, X, x(gap, nonterminal, close, X)) & \text{ :- } \\
& \text{virtual}(\text{close}, XO, X). \\
\end{align*}

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