Ab initio properties of Li-Group-II molecules for ultracold matter studies

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We perform a systematic investigation of the electronic properties of the \( \Sigma^+ \) ground state of Li-alkaline-earth dimers. These molecules are proposed as possible candidates for quantum simulation of lattice-spin models. We apply powerful quantum chemistry coupled-cluster method and large basis sets to calculate potential energies and permanent dipole moments for the LiBe, LiMg, LiCa, LiSr, and LiYb molecules. Agreement of calculated molecular constants with existing experimental data is better than or equal to 8%. Our results reveal a surprising irregularity in the dissociation energy and bond length with an increase in the reduced mass of the molecule. At the same time the permanent dipole moment at the equilibrium separation has the smallest value between 0.01 a.u. and 0.1 a.u. for the heaviest (LiSr and LiYb) molecules and increases to 1.4 a.u. for the lightest (LiBe), where 1 a.u. is one atomic unit of dipole moment. We consider our study of the \( \Sigma^+ \) molecules a first step towards a comprehensive analysis of their interactions in an optical trap.

I. INTRODUCTION

There is growing interest in molecules formed by one alkali-metal atom and one alkaline-earth or rare-earth atom [1–11]. In contrast to group I or group II diatomic molecules, these molecules have an unpaired electron that allows for manipulation of the \( \Sigma^+ \) ground-state molecule with both electric and magnetic external fields. Moreover, it has been suggested that \( \Sigma^+ \) molecules are good candidates in which to explore controlled chemical reactions at ultracold temperatures [2]. The unpaired spin in the ground state of these molecules should provide a new handle for the control of the reaction dynamics based on the interplay between intramolecular spin-rotation couplings. In addition, when placed in an optical lattice, these polar molecules can interact with each other via both electric dipole-dipole and magnetic spin-spin forces. It is therefore possible to engineer unusual forms of interactions for quantum simulation of lattice-spin models and topological quantum computing [11], controlled preparation of many-body entangled states [3], and high-precision measurements of fundamental constants [13].

Another interest in Li-group II molecules stems from prospects to achieve optical Feshbach tuning of scattering properties in ultracold gases of the individual atoms without substantial loss of atoms from a trap. This photoassociative tuning, pioneered for homonuclear molecules [14–21], becomes possible due to the existence of long-lived excited molecular states near narrow intercombination lines of the alkaline-earth or rare-earth atoms. In turn, this might enable efficient ways to form gases of polar molecules without substantial loss by photoassociation. In essence, a two-photon optical Feshbach resonance can be used to couple two colliding atoms to a vibrational level of the molecular ground state. The suppressed effect of excited-state spontaneous decay makes efficient coherent molecular formation possible. Knowledge of the electronic and ro-vibrational properties of the molecules will help to find optimal pathways. Characteristics such as the permanent dipole moments of the ground state will determine the anisotropic interactions between these molecules in an optical trap.

Some key theoretical predictions of the electronic structure and dipole moment of the ground and low-lying excited states of LiYb [8, 9] and for the ground state of LiSr [6] have recently been obtained. Other work has studied RbYb [2] and RbSr [5]. However, the physical origin of the chemical bond of these mixed species is not yet fully understood. Continued theoretical advances are necessary to unravel the properties of these molecular systems. To the best of our knowledge, only the LiMg and LiCa ground states were experimentally investigated [11, 22, 23], which allows us to compare our predictions with experimentally obtained molecular parameters [11, 23]. There are several experimental groups working to achieve the formation of the LiYb molecules at ultracold temperatures [7, 10]. An understanding and quantitative description of these molecules might help to
Our theoretical study is devoted to a systematic investigation of the \(X^2\Sigma^+\) ground state properties of the polar Li-alkaline-earth dimers such as LiBe, LiMg, LiCa, LiSr, and the rare-earth dimer LiYb. These are interesting and challenging systems as the valence electrons of the atoms form a relatively weak covalent bond. The alkaline-earth atom has a closed outer electron shell and a Hartree-Fock interaction energy results in a purely repulsive potential curve. We use the unrestricted (U) or partially spin-restricted (R) coupled cluster (CC) method with either single and double excitations augmented with perturbatively calculated triples (CCSD(T)) or with single, double, and triple excitations (CCSDT) to treat the correlations of core and valence electrons. All approaches are used in conjunction with correlation-consistent basis sets. The dipole moment is calculated using a finite field approach with a four-point numerical differentiation formula. The calculations are performed with CFOUR and MOLPRO suites of programs.

Presumably, the CCSDT method is more accurate in the description of the potential energy surface than the CCSD(T) method, where triple excitations are treated perturbatively. The results of the unrestricted (U) method are more accurate than that of a restricted (R) calculation. The CC method is based on a single-reference configuration and is not suitable for molecules where multiple-configurations are relevant. A practical indicator of how well the CC method performs is based on T1 diagnostics. Our calculation shows that T1 is small and varies from 0.015 to 0.035. This indicates that a single-reference method is valid for these dimers. In fact, a small T1 for all interatomic separations implies that the long-range interaction potentials as well as the dissociation energies can be accurately described.

Our results include the ground-state potential curve, bond distance, harmonic frequency, dissociation energy, and permanent dipole moment for LiBe, LiMg, LiCa, LiSr, and LiYb. For completeness, we calculate vibrational energies of the ground-state potentials. Due to limitations in computational resources we were not able to obtain results for all methods, basis sets, and Li-X dimers. The most accurate potential energy curves and dipole moments are presented in the figures and tables with the exception of Tab. 7, which compares molecular constants obtained with the various methods and basis sets.

All potentials are corrected for basis set superposition errors (BSSE) using the counterpoise procedure of Boys and Bernardi. The sign of the dipole moment depends on the position of the origin. We apply the following convention throughout the paper: The alkaline-earth/rare-earth atom is positioned at the origin and the Li atom moves along the positive \(x\)-axis. A positive sign of the dipole moment corresponds to the charge transfer from the Li atom towards the alkaline-earth/rare-earth atom.

## A. LiBe molecule

There exist several theoretical calculations of the \(X^2\Sigma_{1/2}^+\) electronic ground state of the LiBe molecule. Jones used a density functional formalism based on a local density approximation to predict molecular constants of the LiBe, LiMg, and LiCa molecules. Their dissociation energy is \(D_e/(\hbar c) = 3705.9\ \text{cm}^{-1}\), while the equilibrium bond length \(R_e = 4.90\text{a}_0\) and the vibrational constant \(\omega_e/(\hbar c) = 340\ \text{cm}^{-1}\). Such strong bonding of the LiBe molecule was explained by substantial electron-charge transfer between s and p orbitals. More advanced MRCI calculations of the low-lying doublet and quartet states of LiBe was performed by Fischer et al. In this calculation the ground state is bound by 2497.5 cm\(^{-1}\), \(R_e = 4.95\text{a}_0\), and \(\omega_e/(\hbar c) = 302\ \text{cm}^{-1}\). The permanent dipole moment is \(d_e = 0.95\ \text{a}_u\) at \(R_e\). Another MRCI calculation using all single and double excitations obtained \(D_e/(\hbar c) = 2336.35\ \text{cm}^{-1}\), \(R_e = 4.927\text{a}_0\), and \(\omega_e/(\hbar c) = 300\ \text{cm}^{-1}\), which are close to those of Ref. The effect of inner-shell correlations on the molecular electronic structure was investigated. Later an \(ab\ initio\) configuration-interaction study was reported by Marino and Ermel. Their value of the dissociation energy \(D_e/(\hbar c)=2014\ \text{cm}^{-1}\) is smaller than that in previous studies. In summary, the previous theoretical calculations disagree on dissociation energy and dipole moment values but have much better agreement on the value of the bond length. Our goal is to test results of the previous predictions by performing a coupled cluster calculation accounting for high-order correlation effects.

In our calculation the UCCSD(T) method is used to obtain the ground state potential and dipole moment of LiBe as a function of interatomic separation \(R\). These characteristics are calculated with the large basis set (aug-cc-pV5Z-DK) of Prascher et al., which includes scalar relativistic effects accounted for by the Douglass-Kroll Hamiltonian. Atomic basis sets include \((15s8p5d4f3g2h)\) primitive Gaussian and \(\{7s6p5d4f3g2h\}\) constructed functions for Li and \(\{15s9p5d4f3g2h\}/\{7s6p5d4f3g2h\}\) for Be.

Results of our calculation are shown in Figure Comparing our data with results available from other theories and experiments we conclude that \(R_e = 4.87\text{a}_0\) is close to the experimental measurement of \(R_e = 4.894\text{a}_0\), while the well depth \(D_e/(\hbar c) = 2406.89\ \text{cm}^{-1}\) is in best agreement with the prediction of . In Ref. no value of \(R_e\) is given. The dipole moment value \(d_e = 1.41\ \text{a}_u\) at the equilibrium separation is even larger than that of . The permanent dipole moment averaged over the ground state vibrational wave function is equal to 1.37 \(\text{a}_u\). It is slightly lower than the value of the dipole moment function at \(R = R_e\). The LiBe molecule has the largest dipole moment of the molecular systems considered in this work.

Bound states of \(^7\text{Li}\)\(^9\text{Be}\) are calculated using a discrete
variable representation (DVR) and their binding energies are presented in Table I. The zero-point energy is found to be $D_0/(hc) = 2254.29$ cm$^{-1}$.

### B. LiMg molecule

To the best of our knowledge, there exist two experimental investigations of the LiMg ground state properties $^{[22]}$ $^{[23]}$. The study in Ref. $^{[23]}$ provides molecular constants that we can use for comparison with our calculation. This work was based on resonant photon-ionization spectroscopy of LiMg in the gas phase and gives an accurate bond energy $D_0/(hc) = 1330$ cm$^{-1}$, equilibrium separation $R_e = 5.9a_0$, and vibrational frequency $\omega_e/(hc) = 190$ cm$^{-1}$. A density functional study in Ref. $^{[29]}$ of LiMg gives $D_e/(hc) = 1371$ cm$^{-1}$, $R_e = 6.04a_0$, and $\omega_e/(hc) = 180$ cm$^{-1}$. A MRCI approach with large contracted basis sets and multiple sets of polarization functions is used in Ref. $^{[23]}$ to give predictions for the LiMg ground state molecular constants $D_e/(hc) = 1611.28$ cm$^{-1}$, $R_e = 5.88a_0$, and $\omega_e/(hc) = 183$ cm$^{-1}$. The value for $D_e$ significantly differs from both Ref. $^{[29]}$ and experiment.

Here we apply RCCSD(T) and UCCSD(T) methods with two different basis sets to calculate the potential and dipole moment of the LiMg ground state. Augmented polarized core-valence (aug-cc-pCVQZ) basis sets with Li: $(15s9p5d3f1g)/[7s6p4d3f2g]$ and Mg: $(19s15p6d4f2g)/[9s8p6d4f2g]$ functions $^{[24]}$ $^{[35]}$ are applied in the UCCSD(T) calculation. The calculation is optimized for scalar relativistic calculations of the all-electron Douglas-Kroll Hamiltonian. A comparison with the molecular constants measured in Ref. $^{[23]}$ shows that our $D_0$ and $R_e$ values are in good agreement with this experiment. Figure 2 shows the $R$-dependent potential and dipole moment.

In Table II we present a complete list of $N = 0$ bound states of the $X^2\Sigma^+$ ground state potential of $^7$Li$^{24}$Mg obtained by a DVR calculation. The zero-point corrected energy is found to be $D_0/(hc)=1330.05$ cm$^{-1}$ in agreement with experimental measurement $^{[29]}$.

### TABLE I: All vibrational energies of the $^7$Li$^{24}$Be $X^2\Sigma^+$ ground state potential for the rotational state $N = 0$.

| $\nu$ | Energy/(hc) (cm$^{-1}$) | $\nu$ | Energy/(hc) (cm$^{-1}$) |
|------|------------------------|------|------------------------|
| 0    | -2254.29               | 9    | -337.24                |
| 1    | -1954.76               | 10   | -243.42                |
| 2    | -1669.25              | 11   | -169.45                |
| 3    | -1407.21             | 12   | -112.19                |
| 4    | -1167.64              | 13   | -68.88                 |
| 5    | -951.37              | 14   | -37.48                 |
| 6    | -760.21              | 15   | -16.55                 |
| 7    | -594.38              | 16   | -4.86                  |
| 8    | -453.64              | 17   | -0.50                  |

### TABLE II: All vibrational energies of the $^7$Li$^{24}$Mg $X^2\Sigma^+$ ground state potential for the $N = 0$ rotational state. The potential is based on the RCCSD(T) calculation.

| $\nu$ | Energy/(hc) (cm$^{-1}$) | $\nu$ | Energy/(hc) (cm$^{-1}$) |
|------|------------------------|------|------------------------|
| 0    | -1330.05              | 10   | -216.21                |
| 1    | -1164.35              | 11   | -164.06                |
| 2    | -1010.96              | 12   | -120.16                |
| 3    | -870.00               | 13   | -83.91                 |
| 4    | -741.52               | 14   | -54.87                 |
| 5    | -625.41               | 15   | -32.62                 |
| 6    | -521.43               | 16   | -16.78                 |
| 7    | -429.16               | 17   | -6.89                  |
| 8    | -348.00               | 18   | -1.75                  |
| 9    | -277.27               | 19   | -0.12                  |
apply two coupled-cluster approaches, UCCSD(T) and UCCSDT, that allow us to introduce higher-order correlation effects. To probe the influence of basis sets on the LiCa characteristics we used two different basis sets for each atom. These are all-electron basis sets with quadruple-zeta quality. Basis sets (def2-QZVPP) for Li:((15s6p2d1f)/[6s4p2df1f]) and Ca:((24s18p6d3f)/[11s6p4df3f]) functions are taken from Ref. [41]. Basis sets (aug-cc-pCVQZ) with Li:((15s9p5d3f1g)/[8s7p5df3fg]) and Ca:((25s19p10d4f2g)/[10s9p7df4fg]) functions include larger correlation expansions.

We find that the molecular characteristics depend not only basis set but also on the number of correlated electrons $n_{\text{ct}}$. For example, for a 3-electron correlation one $2s^1$ valence electron of Li and two $4s^2$ valence electrons of Ca are correlated, whereas for 13-electron correlation all electrons of Li and ten $3s^2p^6$ electrons of Ca are included in the active space. We conclude that using the UCCSD(T) method and the more advanced basis set (aug-cc-pCVQZ) leads to an increase of $D_e/(hc)$ and $d_e$ by $\approx 5\%$. For the UCCSDT method we expect similar trends. We believe that the UCCSDT calculation with the basis set (aug-cc-pCVQZ) provides the most accurate electronic potential and dipole moment. These are shown in Fig. [3]. Moreover, this calculation is in a good agreement with the experimental molecular constants reported by Ref. [11].

The upper panel of Fig. [3] shows the potential energy curve of the X $^2\Sigma^+$ state of LiCa as a function of interatomic separation. The permanent dipole moment of this state as a function of $R$ is presented in the lower panel. A complete list of the $N=0$ vibrational energies of the ground state is presented in Table III.

TABLE III: All vibrational energies of the $^7\text{Li}^{40}\text{Ca}$ $X^2\Sigma^+$ ground state potential for the rotational state $N=0$. The potential is based on the UCCSD(T)/aug-cc-pCVQZ calculation.

| $\nu$ | Energy/(hc) (cm$^{-1}$) | $\nu$ | Energy/(hc) (cm$^{-1}$) |
|-------|----------------------|-------|----------------------|
| 0     | -2428.02             | 14    | -442.18              |
| 1     | -2232.09             | 15    | -366.32              |
| 2     | -2042.75             | 16    | -298.77              |
| 3     | -1861.87             | 17    | -239.22              |
| 4     | -1688.77             | 18    | -187.31              |
| 5     | -1524.31             | 19    | -142.70              |
| 6     | -1368.30             | 20    | -105.03              |
| 7     | -1221.05             | 21    | -73.95               |
| 8     | -1082.74             | 22    | -49.08               |
| 9     | -953.39              | 23    | -30.02               |
| 10    | -833.10              | 24    | -16.33               |
| 11    | -721.92              | 25    | -7.41                |
| 12    | -619.79              | 26    | -2.47                |
| 13    | -526.60              | 27    | -0.42                |
To our knowledge there exist no data on the LiSr ground-state potential based on experimental observation. We are only able to compare our results to the theoretical results of Ref. [6]. The calculation of Ref. [6] uses an effective core and core polarization potentials that are incorporated in a configuration-interaction approach. Their molecular constants are $R_e = 6.57\, a_0$, $D_e/(h\,c) = 2587\, \text{cm}^{-1}$, $\omega_e/(h\,c) = 184.9\, \text{cm}^{-1}$, $B_e/(h\,c) = 0.21\, \text{cm}^{-1}$, and $d_e = 0.13\, \text{a.u.}$ In the present study we use different computational methods to predict these characteristics.

We perform calculations for LiSr that are similar to those for LiCa. We use UCCSD(T) and UCCSDT methods with three different basis sets. The inner electrons of the closed 1$s^22s^2\ldots3d^{10}$ shells of Sr are chemically inactive and excluded from the correlation calculation. The 1$s^22s^2$ electrons of Li and the ten 5$s^24s^24p^6$ electrons of Sr, are included in the all-order correlation calculation.

In the first calculation we use the basis set def2-QZVPP with Li:$(15s6p2d1f)/[6s4p2d1f]$ and Sr:$(8s8p5d3f)/[7s5p4d3f]$ functions [41] and the Stuttgart ECP28MDF relativistic effective core potential (ECP) [40]. Finally, we performed a calculation with a more-advanced all-electron basis set (aug-cc-pCV5Z) described by Li:$(18s12p7d5f3g1h)/[10s8p7d4f1g]$ and Sr:$(23s19p12d4f2g)/[11s10p7d4f2g]$ functions from [35]. The UCCSDT calculation is time consuming and has been performed for basis set “[42]” only.

Results of the most advanced calculation by the UCCSDT method with the basis set “[42]” and the UCCSD(T) method with basis set (aug-cc-pCV5Z) are shown in Fig. 4. We see that the potential energy of the two calculations nearly coincide, whereas the dipole moment curves in the bottom panel are slightly shifted relative to each other. We believe that this difference is within the accuracy of our calculation. The largest discrepancy of about 7% with the results of Ref. [6] occurs at large internuclear separation, whereas at $R_e$ the dipole moment $d_e$ differs by 2% to 3% only.

The DVR calculation of the bound state energy gives $D_0/(h\,c) = 2275.59\, \text{cm}^{-1}$ and $\omega/(h\,c) = 182.2\, \text{cm}^{-1}$. Table IV lists all $N = 0$ bound-state energies for $^7\text{Li}^{88}\text{Sr}$. 

D. LiSr molecule
TABLE IV: All vibrational energies of the $^7$Li$^{88}$Sr $X^2\Sigma^+$ ground state potential for the rotational state $N = 0$. The potential is based on the UCCSD(T) calculation with basis set [35].

| $\nu$ | Energy/(hc) (cm$^{-1}$) | $\nu$ | Energy/(hc) (cm$^{-1}$) |
|-------|-------------------------|-------|-------------------------|
| 0     | -2275.59                | 15    | -397.78                 |
| 1     | -2099.56                | 16    | -331.60                 |
| 2     | -1931.06                | 17    | -272.33                 |
| 3     | -1769.35                | 18    | -219.76                 |
| 4     | -1614.41                | 19    | -173.66                 |
| 5     | -1466.66                | 20    | -133.76                 |
| 6     | -1326.14                | 21    |  -99.83                 |
| 7     | -1192.91                | 22    |  -71.56                 |
| 8     | -1067.12                | 23    |  -48.65                 |
| 9     |  -948.89                | 24    |  -30.80                 |
|10     |  -838.24                | 25    |  -17.64                 |
|11     |  -735.17                | 26    |    -8.73                |
|12     |  -639.65                | 27    |    -3.42                |
|13     |  -551.65                | 28    |    -0.86                |
|14     |  -471.08                | 29    |     -0.04               |

E. LiYb molecule

Recently, two extensive quantum-chemical calculations of the ground and excited states of the LiYb molecule have been reported by Zhang et al. [8] and by Gopakumar et al. [9]. The first calculation used both MRCI and UCCSD(T) methods. Scalar relativistic effects were included by the Douglas-Kroll-Hamiltonian and an effective core potential. Their molecular constants for the $X^2\Sigma^+$ ground state of $^7$Li$^{172}$Yb are the following: $R_e = 6.681 a_0$, $D_e/(hc) = 1577$ cm$^{-1}$, $\omega_e/(hc) = 147.36$ cm$^{-1}$. Different treatments of the Yb core electrons lead to different values of the dipole moment. A RECP-pseudo-potential calculation gave $d_e = 0.022$ a.u., while an all-electron DKH3 calculation gave a smaller $d_e$ of 0.011 a.u. Results of a calculation by [9] were based on both the CASPT2 perturbation theory and the CCSD(T) method. Relativistic effects were taken into account through the Douglas-Kroll-Hess Hamiltonian. Their best values of molecular constants are: $R_e = 6.669 a_0$, $D_e/(hc) = 1421.96$ cm$^{-1}$, $\omega_e/(hc) = 135.54$ cm$^{-1}$.

Our goal here is to perform an independent calculation of the ground state potential and permanent dipole moment of LiYb using the UCCSD(T) method with another effective ECP28MWB pseudo-potential and with basis sets for Li: (15s6p2d1f)/[6s4p2d1f] and Yb: (14s13p10d8f6g)/[10s8p5d4f3g] functions from [44].

Results of our calculation are shown in Fig. 5. The upper panel of Fig. 5 shows the ground state potential of LiYb, which is significantly deeper than the potentials obtained in Refs. [8, 9]. The permanent dipole moment is presented in the bottom panel. It is small and agrees well with the DKH3 value of Ref. [8].

Table V shows all $N = 0$ bound-state energies for $^7$Li$^{172}$Yb.

II. SUMMARY

The objective of our research has been a systematic investigation of the $X^2\Sigma^+$ ground state properties of Li-group II molecules. To achieve this goal we applied powerful quantum chemistry UCCSD(T) and UCCSDT methods with large basis sets to calculate potential energies and permanent dipole moments. Table VI displays molecular constants obtained in our calculations.

Figures 6 and 7 and Table VI summarize our results. Figure 6 reveals a most striking irregularity in the dissociation energy and $R_e$ among the Li-group II molecules. The deepest and most shallow potentials belong to the LiCa and LiMg molecules, respectively. Figure 7 shows dipole moment functions for all molecules considered in our study. There is some consistency in the maximum value of $d$ with the reduced mass of the molecule: heavier molecules have smaller dipole moment. The dipole moment averaged over the ground state vibrational wave function is always a few tenths of atomic units smaller than $d_e$. The LiSr and LiYb molecule have the smallest dipole moments among all molecules in this study.
Table VI presents molecular constants calculated by the RCCSD(T), UCCSD(T) and UCCSDT methods using several large basis sets available in the literature. Comparison of our most accurate (either UCCSD(T) or UCCSDT) calculations with existing experimental measurements of the molecular constants shows that we are able to reproduce the bond length ($R_e$), harmonic frequency ($\omega_e$), and dissociation energy ($D_e$) within 5%, 8%, and 6%, respectively.

The dipole moment as a function $R$ is calculated in terms of a charge transfer and induced charge transfer. These two contributions have opposite signs over a large range of internuclear separations. We conclude from our calculations that charge transfer from the Li-atom to the alkaline-earth atom prevails at all separations. This trend is reversed for LiYb at $R > 7a_0$.

We also highlight the importance of the correlation effects in calculations of the alkali-alkaline-earth molecules. We have gathered numerical evidence to show that molecular constants of these molecules, such as dissociation energy and permanent dipole moment of the ground state, are extremely sensitive to high order correlations. We believe that the best values of these characteristics are obtained by using the UCCSDT method, where correlation effects are taken into account at all orders.

Finally, we want to emphasize that LiBe and LiMg are not likely candidates for ultracold studies because of the difficulty of cooling Be or Mg. However, LiCa looks quite promising, since a Ca BEC [45] has been made, and its dipole moment is comparable to the known RbCs case [46]. The $^2\Sigma^+$ ground state gives an extra spin degree of freedom relative to the $^1\Sigma^+$ RbCs species, thus
TABLE VI: Molecular constants for the $X^2\Sigma^+_{\pm}$ state of LiBe, LiMg, LiCa, LiSr, and LiYb obtained by the RCCSD(T), UCCSD(T) and UCCSDT methods. Here, $1 \, a_0 = 0.0529177$ nm is the Bohr radius and a dipole moment of 1 a.u. corresponds to $1 \, e\, a_0$, where $e$ is the electron charge. Also $\hbar$ is Planck’s constant and $c$ the speed of light.

| Description | $R_e$ | $\omega_e/(hc)$ | $D_e/(hc)$ | $d_e$ |
|-------------|-------|-----------------|------------|-------|
| $^7\text{Li}^9\text{Be}$ | | | | |
| RCCSD(T) | | | | |
| aug-cc-pV5Z-DK | 4.873 | 299.5 | 2406 | 1.41 |
| Experiment \[22\] | 4.894 | | | |
| UCCSD(T) | | | | |
| \coefficient{RCCSD(T)} | | | | |
| aug-cc-pV5Z-DK | 5.87 | 206.1 | 1432 | 0.44 |
| Experiment \[23\] | 5.9 | 190 | 1423$^a$ | |
| $^7\text{Li}^{24}\text{Mg}$ | | | | |
| RCCSD(T) | | | | |
| aug-cc-pCVQZ | 5.86 | 174.4 | 1417 | 0.32 |
| UCCSD(T) | | | | |
| \coefficient{RCCSD(T)} | | | | |
| aug-cc-pV5Z-DK | 5.87 | 206.1 | 1432 | 0.44 |
| Experiment \[23\] | 5.9 | 190 | 1423$^a$ | |
| $^7\text{Li}^{40}\text{Ca}$ | | | | |
| RCCSD(T) | | | | |
| \coefficient{UCCSD(T)} | | | | |
| aug-cc-pCVQZ | 6.357 | 207.1 | 2607 | 0.440 |
| UCCSDT | | | | |
| \coefficient{UCCSD(T)} | | | | |
| aug-cc-pCVQZ | 6.357 | 207.1 | 2607 | 0.440 |
| Experiment \[11\] | 6.3415(5) | 195.2 | 2607.8(100) | |
| $^7\text{Li}^{88}\text{Sr}$ | | | | |
| RCCSD(T) | | | | |
| \coefficient{UCCSD(T)} | | | | |
| def2-QZVPP | 6.766 | 167.0 | 2165 | 0.109 |
| basis of \[42\] | 6.712 | 183.0 | 2302 | 0.117 |
| aug-cc-pCVQZ | 6.700 | 182.2 | 2367 | 0.112 |
| UCCSDT | | | | |
| \coefficient{UCCSD(T)} | | | | |
| def2-QZVPP | 6.711 | 184.2 | 2401 | 0.096 |
| basis of \[42\] | | | | |
| $^7\text{Li}^{172}\text{Yb}$ | | | | |
| RCCSD(T) | | | | |
| \coefficient{UCCSD(T)} | | | | |
| basis of \[14\] | 6.710 | 181.5 | 2289 | 0.011 |

$^a$This value is estimated from $D_0$ of Ref. \[23\]

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