A continental-scale evaluation of the calibration-free complementary relationship with physical, machine-learning, and land-surface models

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Abstract. The widespread negative correlation between the atmospheric vapor pressure deficit and soil moisture lends strong support to the complementary relationship (CR) of evapotranspiration. While it has showed outstanding performance in predicting actual evapotranspiration (ETa) over land surfaces, the calibration-free CR formulation has not been tested in the Australian continent dominantly under (semi-)arid climates. In this work, we comparatively evaluated its predictive performance with seven physical, machine-learning, and land surface models for the continent at a 0.5°×0.5° grid resolution. Results showed that the calibration-free CR that forces a single parameter to everywhere produced considerable biases when comparing to water-balance ETa (ETwb). The CR method was unlikely to outperform the other physical, machine-learning, and land surface models, overrating ETa in (semi-)humid coastal areas for 2002-2012 while underestimating in arid inland locations. By calibrating the parameter against water-balance ETa independent of the simulation period, the CR method became able to outperform the other models in reproducing the spatial variation of the mean annual ETwb and the interannual variation of the continental means of ETwb. However, interannual the grid-scale variability and trends were captured unacceptably even after the calibration. The calibrated parameters for the CR method were significantly correlated with the mean net radiation, temperature, and wind speed, implying that (multi-)decadal climatic variability could diversify the optimal parameters for the CR method. The other physical, machine-learning, and land surface models provided a consistent indication with the prior global-scale assessments. We also argued that at least some surface information is necessary for the CR method to describe long-term hydrologic cycles at the grid scale.

1 Introduction

Terrestrial evapotranspiration (ETa) links water, energy, and carbon exchanges between lands and the atmosphere. On the global scale, more than 60% of land precipitation (P) returns to the atmosphere through plants’ vascular systems and soil pores, consuming over 70% of surface net radiation for the phase change of water (Trenberth et al., 2009; 2007). Due to
the warming atmosphere, the upward latent heat flux has received growing attention, because it can control surface water availability, plants productivity, and ecosystem sustainability (Pareek et al., 2020; Kyatengerwa et al., 2020; Jasechko, 2018; Swann et al., 2016). Interacting with the atmosphere, changes in ETa could substantially increase heatwave risks (Miralles et al., 2014a; Mueller and Seneviratne, 2012) and alter precipitation patterns (Koster et al., 2004).

However, expensive costs and operational difficulties make ETa observation networks (e.g., the FLUXNET; Baldocchi et al., 2001) subject to limited spatial extent, short data lengths, and questionable data quality. Hence, modeling approaches are inevitable for a regional- or a global-scale ETa analysis, and usually based on physical theories (e.g., Zhang et al., 2016), machine-learning techniques (e.g., Jung et al., 2011), and conceptual land surface schemes (e.g., Haverd et al., 2018) that inherently have numerous error sources. For instance, Jung et al. (2019) produced the global mean ETa from 557 to 668 mm a⁻¹ for 2001-2005 with physical and machine learning models. The previous global mean ETa estimates have varied even in a larger range of 417-650 mm a⁻¹ for a part or the whole period of 1982-2011 (Pan et al., 2020). The large discrepancies in the global means imply that modeling prescriptions for ETa have diverse uncertainty sources, such as forcing errors, ill-posed parameterizations, structural deficiencies, and insufficient training, and thus necessitate intercomparison studies to assess the associated limitations and uncertainties (e.g., Pan et al., 2020).

When it depends on a physical equation, such as the Penman-Monteith (Monteith, 1965) or the Priestley-Taylor (Priestley and Taylor, 1972) equations, an ETa model assumes typically that ETa under water deficiency is proportional to the atmospheric evaporative demand (ETp). In the Global Land Evaporation Amsterdam Model (GLEAM; Martens et al., 2017), for example, the Priestley-Taylor equation is multiplied by a stress module to predict ETa under water limited conditions. Similar approaches are easily found with physical and land surface models that adjust the surface roughness length of the Penman-Monteith equation to represent water stress (e.g., Zhang et al., 2016; Pan et al., 2015). Note that adjusting the surface roughness length is mathematically equivalent to multiplying a coefficient to ETp (Seneviratne et al., 2010). Though it has reliably predicted ETa at multiple scales (e.g., Martens et al., 2017; Fisher et al., 2008), the proportionality assumption unavoidably requires soil moisture information to quantify the degree of water stress, giving rise to practical difficulties such as data unavailability, computational inefficiency, and delayed data dissemination. Importantly, the assumption of the positive relation between ETa and ETp could be rejected by observational evidence that supports negative correlations between the two (e.g., Brutsaert, 2006; Ramírez et al., 2005; Hobbins et al., 2004). Han et al. (2014) emphasized that the correlation between ETa and ETp depends mainly on water availability rather than being always positive.

The drawbacks of the proportionality assumption can be remedied at least in part by employing the complementary relationship (CR) of evapotranspiration. Bouchet (1963) found that the pan evaporation rate over a small wet patch surrounded by water-limited areas is higher than when the same surroundings are entirely wet. Since the small wet patch hardly influences the overlying atmosphere, ETp over the wet surface is raised by blending with the drier and hotter surroundings. This “oasis effect”, by contrast, is negligible in the case that the surrounding areas are entirely wet and large enough to transform the overpassing atmosphere. In other words, even under the same surface radiation and wind speed conditions, ETp responds to changes in regional water availability. Hence, one can predict water-limited ETa by gauging how much ETp is raised from the
hypothetical evaporation rate that should occur under the full wetness (referred to as the wet-environment ET; $\text{ET}_w$). Since a higher adjustment in $\text{ET}_p$ indicate a lower water availability and thus $\text{ET}_a$, the CR supports inverse correlations between $\text{ET}_a$ and $\text{ET}_p$ (i.e., complementarity). In practice, the complementarity allows users to predict $\text{ET}_a$ with no surface information, because $\text{ET}_p$ and $\text{ET}_w$ are all obtainable from meteorological data.

After Brutsaert and Parlange (1998) who used the CR to interpret the globally declining pan evaporation rates, various CR methods have been formulated, e.g., Anayah and Kaluarachchi (2014), Crago and Qualls (2013), Huntington et al. (2011), Kahler and Brutsaert (2006), Crago and Crowley (2005), Hobins et al. (2004) among others. While those CR methods have been deemed mere heuristic methods with limited reliability (Shuttleworth et al., 2009), the non-dimensional derivation of Brutsaert (2015) and the following modifications (Szilagyi et al., 2017; Crago et al., 2016) have suggested the generality and definitiveness of the CR principle. The non-dimensional CR formulations have shown outstanding performance in predicting water-limited $\text{ET}_a$ at local, regional, and global scales (e.g., Brutsaert et al., 2020; Crago and Qualls, 2018; Brutsaert et al., 2017), and applications are extended to drought assessments (Kyatengerwa et al., 2020; Kim et al., 2019b) and even used for predicting the crop coefficient under the proportionality assumption (Kim et al., 2019a).

Though the non-dimensional CR formulations are still under improvement based on the thermodynamic foundations (Szilagyi, 2021; Qualls and Crago, 2020), they mostly require any $\text{ET}_a$ observations to identify required parameters. Szilagyi et al. (2017) is the only calibration-free CR method that analytically determines the parameter for $\text{ET}_w$ with no requirement of $\text{ET}_a$ data. By transferring the parameter analytically obtained in highly humid locations to the entire region of interest, the calibration-free CR formulation showed superior performance in predicting $\text{ET}_a$ to typical land surface and machine-learning models in the conterminous United States and China where climates are very diverse (Ma et al., 2019; Ma and Szilagyi, 2019). However, the same approach has not been examined in a continent where only small parts are under humid climates, and thus it is questionable whether the parameter transferring from humid locations is valid.

In this work, therefore, we applied the calibration-free CR formulation for the Australian continent where land surfaces are mostly under (semi-)arid climates, and its predictive performance was compared with a bunch of physical, machine-learning, and land surface models. Here, we addressed that the use of a single parameter for the entire continent could lead the CR method to low performance in preserving spatial coherence, interannual variability, and decadal trends of water-balance $\text{ET}_a$. We also provided some perspectives for improving the non-dimensional CR formulations.

### 2 Methodology and data

#### 2.1 The generalized complementary relationship approach

The CR principle explains the feedback response of $\text{ET}_p$ to regional water deficiency using the three evaporation rates, namely, $\text{ET}_w$, $\text{ET}_p$, and $\text{ET}_a$. Again, $\text{ET}_a$ is the actual water flux from a homogeneous land surface to the atmosphere, and $\text{ET}_p$ is the atmospheric capacity to receive water vapor that responds actively to water availability on the surface. $\text{ET}_w$ is the hypothetical $\text{ET}_a$ rate that would take place under the same atmospheric conditions but ample water. $\text{ET}_p$ under regional water
deficiency would be far higher than the hypothetical ETw, because high atmospheric vapor pressure deficits (VPD) co-exist with low soil moisture across the globe (Zhou et al., 2019).

In the CR formulation by Szilagyi et al. (2017), the two dimensionless variables, \( x \equiv ET_w/ET_p \) and \( y \equiv ET_a/ET_p \), are defined, and they are linked with four boundary conditions. If water is ample on the surface, \( ET_a \) reaches \( ET_w \) that should be equal to \( ET_p \) owing to no water deficiency; thus, the first boundary condition is (i) \( y = 1 \) for \( x = 1 \). When the surface is entirely desiccated, \( ET_a \) must be nil (i.e., \( y = 0 \)), and by energy balance, the surface radiation should be fully transformed to the sensible heat flux that fully amplifies VPD. In other words, under the given radiation and wind speed, \( ET_p \) is maximized when \( ET_a = 0 \), providing another zero-order boundary condition: (ii) \( y = 0 \) for \( x = x_{\min} \equiv ET_w/E_{p_{\max}} \), where \( E_{p_{\max}} \) is the maximized \( ET_p \). When \( x = 1 \) (i.e., with ample water), \( ET_a \) would change as much as changes in \( ET_w \), yielding a first-order boundary condition: (iii) \( dy/dx = 1 \) for \( x = 1 \). On the other boundary (i.e., \( x = 0 \)), \( ET_a \) should be constant irrespective of any changes in \( ET_a \); thus, another zero-order boundary condition is (iv) \( dy/dx = 0 \) for \( x = 0 \). The simplest polynomial equation satisfying the four boundary conditions is:

\[
y = 2X^2 - X^3, \tag{1a}
\]

with \( X \) defined as:

\[
X \equiv \frac{x-x_{\min}}{1-x_{\min}} = \frac{E_{p_{\max}}-ET_p}{E_{p_{\max}}-ET_w} \tag{1b}
\]

Since \( ET_p, ET_w, \) and \( E_{p_{\max}} \) could be all obtainable from a set of net radiation, air temperature and humidity, and wind speed data, Eqs. (1a) and (1b) allow users to estimate \( ET_a \) with no direct soil moisture information (e.g., remote-sensing soil moisture products). Szilagyi et al. (2017) used the Penman (1948) equation for \( ET_p \):

\[
ET_p = \frac{\Delta_{\text{avg}}}{\Delta_{\text{avg}}+\gamma} \frac{R_n}{\Delta_{\text{avg}}+\gamma} + \frac{\gamma}{\Delta_{\text{avg}}+\gamma} f_u VPD, \tag{2}
\]

where, \( \Delta_{\text{avg}} \) is the slope of the saturation vapor pressure curve (kPa °C\(^{-1}\)) at the mean air temperature \( T_{\text{avg}} \) (°C), \( \gamma \) is the psychometric constant (kPa °C\(^{-1}\)), \( R_n \) is the surface net radiation less the soil heat flux (MJ m\(^{-2}\) d\(^{-1}\)), \( \lambda_c \) is the latent heat of vaporization (MJ kg\(^{-1}\)) (here we quantified it by \( \lambda_c = 2.501-0.00236T_{\text{avg}} \)), \( f_u = 2.6(1+0.54u_2) \) is the Rome wind function, where \( u_2 \) is the 2-m wind speed (m s\(^{-1}\)), and VPD is \( e_s(T_{\text{avg}}) - e_a \), where \( e_s(T_{\text{avg}}) \) is the saturation vapor pressure at \( T_{\text{avg}} \) and \( e_a \) is the actual vapor pressure, respectively.

As it is parameterized under wet surface conditions, \( ET_w \) could be quantified by the Priestly and Taylor (1972) equation:

\[
ET_w = \alpha e \frac{\Delta_{ws}}{\Delta_{ws}+\gamma} \frac{R_n}{\Delta_{ws}+\gamma} \tag{3}
\]

where, \( \alpha e \) is a coefficient typically ranging between 1.10 and 1.32 (Szilagyi et al., 2017), and \( \Delta_{ws} \) is the slope of the vapor pressure curve (kPa °C\(^{-1}\)) at the wet surface temperature \( T_{ws} \) for which Szilagyi (2014) used the two methods based on the Bowen ratio and the derivation of Monteith (1980). We used the latter:

\[
T_{ws} = T_{wb} + \frac{\gamma R_n VPD}{(\Delta_{wb}+\gamma)(c_1 R_n + c_2 f_u VPD)}, \tag{4a}
\]
\[ c_1 = \frac{\Delta_{\text{avg}}(\Delta_{wb} + \gamma) - \Delta_{wb}(\Delta_{\text{avg}} + \gamma)}{\Delta_{\text{avg}} + \gamma}, \quad (4b) \]
\[ c_2 = \frac{\lambda_v \gamma(\Delta_{wb} + \gamma)}{\Delta_{\text{avg}} + \gamma}, \quad (4c) \]
where, \( T_{wb} \) is the wet-bulb temperature that can be estimated by the Bowen ratio for an adiabatic change:
\[ \frac{T_{wb} - T_{\text{avg}}}{e_s(T_{wb}) - e_s} = -1. \quad (5) \]

\( E_{\text{pmax}} \) is calculated with the same Penman equation but with different temperature and humidity conditions. The air overpassing a desiccated surface is likely devoid of humidity; thus, \( e_s \) would become negligible:
\[ E_{\text{pmax}} = \frac{\Delta_{\text{dry}}}{\Delta_{\text{dry}} + \gamma} \left( \frac{R_n}{\lambda_v} + \frac{\gamma f_u e_s(T_{dry})}{\Delta_{\text{dry}} + \gamma} \right), \quad (6) \]
where, \( \Delta_{\text{dry}} \) is the slope of the vapor pressure curve (kPa °C\(^{-1}\)) at the dry air temperature \( T_{\text{dry}} \) (°C). \( T_{\text{dry}} \) is the hypothetical air temperature that would adiabatically reach when the latent heat flux is nil:
\[ T_{\text{dry}} = T_{wb} + \frac{e_s(T_{wb})}{\gamma} = T_{\text{avg}} + \frac{e_s(T_{\text{avg}})}{\gamma}. \quad (7) \]

The coefficient \( \alpha_c \) in Eq. (3) is the only parameter for the CR method. Szilagyi et al. (2017) proposed to use the mean value of \( \alpha_c \) values analytically obtained at humid locations for a region of interest, and we achieved \( \alpha = 1.09 \) by the same approach (the details are given in the Appendix). Although it is smaller than the typical Priestley-Taylor coefficient (1.26), the obtained \( \alpha_c \) was still higher than the physical lower limit (i.e., unity). It should be noted that the \( \alpha_c \) incorporated in the CR method is a model parameter analogous to the Priestley-Taylor coefficient rather than having the same physical meaning (Ma et al., 2019; Brutsaert et al., 2017). In prior continental-scale studies, the optimal \( \alpha_c \) values for continental-scale applications were often lower than the typical Priestley-Taylor coefficient (1.26) (e.g., Ma et al, 2020; Kim et al., 2019b; Ma et al., 2019; Ma and Szilagyi, 2019).

### 2.2 Data used for \( \text{ET}_a \) estimation and performance evaluation

#### 2.2.1 Atmospheric forcing and evaluation datasets

The study area was the Australian continent lying within [10°- 45° S, 113°- 155° E], and the atmospheric forcing data for the CR method were collected from the ERA Interim reanalysis archive (Dee et al., 2011) of the European Centre for Medium-Range Weather Forecasts (https://www.ecmwf.int/en/forecasts/datasets/reanalysis-datasets/era-interim; last access on mmm-dd/2020). The monthly averages of surface net solar radiation and net thermal radiation, 2-m air temperature, 2-m dew-point temperature, and 10-m U and V wind speed components were downloaded at the 0.5°×0.5° grid resolution for 1979-2018. \( R_n \) was estimated simply by summing the two net radiation data (i.e., the soil heat flux was assumed to be negligible). \( T_{\text{avg}} \) and VPD were directly quantified by the air temperature and the dew-point temperature datasets, while the 10-m U and V components were converted to \( u_2 \) values using the logarithmic wind speed profile.
The CR ET estimates from Eq. (1a) were evaluated with the water-balance ET (ET\(\text{wb}\)) estimates at the same 0.5° grid resolution. To achieve the grid-scale ET\(\text{wb}\), some syntheses (e.g., spatial and temporal gap filling and/or conceptual modelling) are inevitable due to the non-uniformity and unavailability of in-situ precipitation, streamflow, and terrestrial water storage (TWS) observations. We collected the global precipitation (P) product v.2018 of the Global Precipitation Climate Centre (GPCC) together with the grid runoff (Q) products by Ghiggi et al. (2019) and Hobeichi et al. (2019) and the TWS anomalies reconstructed by Humphrey and Gudmundsson (2019). The GPCC monthly P data are readily available for 1891-present from [https://psl.noaa.gov/data/gridded/data.gpcc.html](https://psl.noaa.gov/data/gridded/data.gpcc.html) (last access on Jun-01/2020). The monthly GRUN was produced by Ghiggi et al. (2019) at the 0.5° resolution for 1902-2014 using in-situ streamflow observations and a machine learning algorithm, and cross-validated by independent discharge data in major river basins across the world ([https://doi.org/10.6084/m9.figshare.9228176](https://doi.org/10.6084/m9.figshare.9228176); last access on May-20/2020). The Linear Optimal Runoff Aggregate (LORA) of Hobeichi et al. (2016) merged the syntheses of eleven land surface models using an optimal weighting approach for 1980-2012 ([https://geonetwork.nci.org.au/geonetwork/srv/eng/catalog.search#/metadata/f9617_9854_8096_5291m](https://geonetwork.nci.org.au/geonetwork/srv/eng/catalog.search#/metadata/f9617_9854_8096_5291m); last access on Dec-23/2020). Hobeichi et al. (2016) validated the LORA Q data with published discharge observations at many river basins. Since we believed that Q values from multiple sources are more reliable than a single model synthesis, the Q value at each grid was determined by simple averages of the GRUN and the LORA data. The TWS data, namely the GRACE-REC, extend the Gravity Recovery and Climate Experiments (GRACE) land water-equivalent-thickness data given for 2003-2015 to the year of 1901 using a statistical methods ([https://doi.org/10.5194/hess-2021-126](https://doi.org/10.5194/hess-2021-126); Preprint. Discussion started: 16 March 2021 © Author(s) 2021. CC BY 4.0 License.). We calculated annual TWS changes (\(\delta S\)) at each grid by differencing the December TWS estimates of two consecutive years. Then, the annual ET\(\text{wb}\) in each year was calculated by the water balance equation, i.e., \(\overline{ET_{\text{wb}}} = \overline{P} - \overline{Q} - \delta S\), where \(\overline{ET_{\text{wb}}}\), \(\overline{P}\), and \(\overline{Q}\) are the annual averages of ET\(\text{wb}\), P, and Q, respectively.

Figure 1 displays the distribution of the wetness index (the long-term-average ratio of P to ET\(\rho\)) for 2002-2012 calculated with the GPCC P and the ET\(\rho\) from the ERA-Interim forcing. Typically, the wetness index categorizes hyper-arid, arid, semi-arid, semi-humid, and humid climates with the thresholds of 0.05, 0.2, 0.5, and 0.65, respectively (Barrow, 1992). The range of the wetness index was 0.07-5.65 in Australia, indicating that 81% of the land surfaces was under (semi-)arid climates though there are no hyper-arid areas. Humid climates are found in northern, southwestern, and southeastern coastal regions, where major cities and agricultural areas have developed.
2.2.2 ET<sub>a</sub> products for comparative evaluation

The performance of the CR method was compared with products from two remote-sensing-based physical models, a machine-learning model, and four land surface schemes. The physical models include the Global Land Evaporation Amsterdam Model (GLEAM) v3.2 (Martens et al., 2017; https://www.gleam.eu; last access on Jun-03/2020) and the Priestley-Taylor Jet Propulsion Laboratory Model (PT-JPL) (Fisher et al., 2008; http://josh.yosh.org/datamodels.htm; last access on Dec-03/2020). The GLEAM uses a vertically-stacked bucket model in combination with the Priestley-Taylor equation constrained by microwave-derived soil moisture, surface temperature, and vegetation optical depth. It synthesizes canopy transpiration, bare-soil evaporation, and interception losses under water- and energy-limited conditions separately. On the other hand, the PT-JPL employs the same Priestley-Taylor equation multiplied with the relative surface wetness from remote-sensing vegetation indices. The GLEAM and the PT-JPL ET<sub>a</sub> products were shown to have high coherence with eddy-covariance latent heat flux observations (Martens et al., 2017; Fisher et al., 2008).

In addition, the FluxCom was selected as the machine-learning ET<sub>a</sub> product (Jung et al., 2019; http://www.fluxcom.org/; last access Mar-18/2019). This dataset was produced by upscaling the point flux-tower observations with 11 machine learning algorithms with remote-sensing vegetation indices. Jung et al. (2019) checked the cross-consistency...
of the FluxCom data via comparison against the model-tree ensemble (Jung et al., 2011), the GLEAM v3.1, and the LandFlux-Eval datasets (Mueller et al. 2013). The FluxCom provides several variations; among them, we chose the dataset forced by the CRUNCEPv8 with the length from 1950 to 2016.

The land surface models include the Australian Water Resources Assessment Landscape Model v.5 (AWRA-L; Frost et al., 2016), the Noah Land Surface Model v.3.3 (Noah3.3; Ek et al., 2003), the Catchment Land Surface Model v. Fortuna 2.5 (CLSMF2.5; Koster et al., 2000), and the ERA-Interim land surface scheme (ERA-Interim; Balsamo, 2008). The AWRA-L is a one-dimensional grid water balance model developed for monitoring water stresses in Australian soil, underground, and land surfaces (http://www.bom.gov.au/water/landscape; last access on Dec-30/2020). The AWRA-L ETa is the sum of interception, soil evaporation, groundwater evaporation, and transpiration from the root zone and deep groundwater generated by a conceptual tank model combining the Penman-Monteith equation. The Noah3.3 and the CLSMF2.5 ETa products were generated via the Land Information System (LIS; Kumar et al., 2006) of the National Aeronautics and Space Administration (NASA), which supports application of multiple community land surface models. The Noah3.3 is the operational land surface scheme of the National Center for Atmospheric Research (NCAR) discretizing the surfaces with the finite difference method and solving the governing equations associated with the soil-vegetation-snowpack continuum. On the other hand, the CLSMF2.5 was developed by the NASA Global Modeling and Assimilation Office, subdividing the irregular shapes of catchments into saturated, sub-saturated, and wilting fractions, and simulating simulates water fluxes in each fraction of catchments that evolves over time. For our comparative evaluation, both the Noah 3.3 and CLSMF2.5 models were forced by the National Centers for Environmental Prediction Global Data Assimilation System (NCEP GDAS) forcing dataset (https://portal.nccs.nasa.gov). The simulation time step and spin-up period were 15 min and 76 years (four times 19 years (2000–2018), respectively. The Hydrologigcal Modeling and Analysis Platform (Getirana et al. 2012) routing scheme was applied for routed streamflow estimates. Lastly, the ERA-Interim uses the improved land surface scheme formulated by Viterbo and Beljaars (1995) to simulate the evolution of heat and water storages in soil and snow layers. It classifies a land surface using satellite data and ancillary information. The downward water fluxes in a land pixel are generated by the governing equations, and the latent heat flux to the lowest atmospheric level is computed with the Obukhov length.

For comparison between the nine ETa products, the different spatial resolutions were bilinearly unified to the standard 0.5° grid of the ERA-Interim forcing data. We compared all the ETa products to the grid-scale ETwb, and evaluated the reproducibility in spatial variation of long-term mean ETa and the continental means together with the grid-scale interannual variability and linear trends.

3 Results

3.1 Evaluation of spatial variations and continental means

Figure 2a illustrates the distribution of long-term ETwb means for 2002-2012. The spatial variation of the mean ETwb was consistent with the analysis of Zhang et al. (2010) for which a typical Budyko function was adopted to produce the mean
ETₐ at 0.05° resolution across Australia for 2000-2005. Despite the different data length and the spatial resolution, Zhang et al. (2010) suggested that that the mean ETₐ in Australia is the lowest in the east-central part receiving very small precipitation. The region with AI < 0.10 in Figure 1 corresponds approximately to where the mean ETₐ is very low in Zhang et al. (2010) and Figure 2a. In the arid Australian continent, the precipitation pattern mostly determines the spatial variation of mean ETₐ, because about 90% of precipitation returns to the atmosphere (Glenn et al., 2011). Figure 2a, too, depicts that the means of ETₐ wb were small in the arid east-central part, increasing towards northern and eastern coasts where precipitation is abundant due to monsoonal and easterly winds. The continental mean ETₐ wb for 2002-2012 was 431 mm a⁻¹ approximately close to the value (439 mm a⁻¹) given by the global assessment of Zhang et al. (2016). The consistency to prior studies led us believe that the annual ETₐ wb product from the reanalysis precipitation and the reconstructed runoff and TWS data could become an acceptable evaluation reference.

As expected, the mean ETₐ wb tended to increase with AI. In arid regions (AI < 0.2), the mean ETₐ wb was 260 ± 71.9 mm a⁻¹ (mean ± standard deviation), while semi-arid regions (0.2 ≤ AI < 0.5) had a range of 489 ± 152 mm a⁻¹. Under semi-humid (0.5 ≤ AI < 0.65) and humid (AI ≥ 0.65) climates, it was within 761 ± 168 mm a⁻¹ and 797 ± 273 mm a⁻¹, respectively. Compared to ETₐ wb, the CR ETₐ had positive biases. The mean ETₐ from the CR method for 2002-2012 ranged in 221 ± 105 mm a⁻¹, 564 ± 231 mm a⁻¹, 976 ± 235 mm a⁻¹, and 1,057 ± 297 mm a⁻¹ from arid to humid regions, respectively (Figure 2b).

Though the pattern correlation between the mean ETₐ wb and CR ETₐ was fairly high (Pearson r was 0.87), the CR method overestimated ETₐ in coastal areas, while underrating it in the central-western part under arid climates.

The two physical models, on the other hand, were biased negatively. The GLEAM produced smaller ETₐ in the wet northern coastal, and the (semi-)arid central and southwestern parts than ETₐ wb, while the PT-JPL seemed to generally underestimated it across the continent (Figure 3c and d). On the contrary, the FLUXCOM product was positively biased in (semi-)arid inland areas with suppressed spatial variation (Figure 3e). The land surface scheme of AWRA-L generated the unexpected dry hotspots in the mid-western part, which was not found from the water balance (Figure 3f). The two LIS land surface models, the Noah3.3 and the CLSMF2.5, relatively well captured the spatial variation of mean ETₐ wb, although there were some underestimations by the Noah3.3 in the northern part (Figure 3g and h). The ERA-Interim ETₐ was of largely biased in coastal areas (Figure 3i).

The continental means ETₐ for 2002-2012 from the eight models provide a consistent indication (Figure 3a). The CR method generated a positive bias of +58.2 mm a⁻¹ (+14%) relative to the water-balance ETₐ wb. Among the eight models, the CLSMF2.5 produced the minimum bias (+0.5%), whereas the largest bias (+24%) was from the ERA-Interim ETₐ. In the Taylor (2001) diagram that measures the standard deviation, and the root mean square error (RMSE) and the pattern correlation to ETₐ wb together, the CR method appeared to be in the 6th rank. The CLSMF2.5 ETₐ was the closest to ETₐ wb, and followed in order by the PT-JPL, the AWRA-L, the FluxCom, the Noah3.3, the CR method, the GLEAM, and the ERA-Interim.

The continental annual means of CR ETₐ were considerably higher than those from ETₐ wb owing to the positive biases in coastal areas, and their interannual variability was smaller than that of ETₐ wb (Figure 4). The GLEAM well captured the interannual variation of the continental mean ETₐ wb through 1981-2012 with slight underestimation; however, the PT-JPL ETₐ
were of considerable negative biases. As did the kindred machine learning model of Jung et al. (2011), the FluxCom suppressed the temporal variation of the annual means. Though the AWRA-L, the Noah3.3, and the CLSMF2.5 appeared to have small biases to the annual means of \( ET_{wb} \), the temporal correlations of the two LIS land surface models to \( ET_{wb} \) were lower than the other models (0.7 and 0.75 for the Noah3.3 and the CLSMF2.5 vs. 0.86-0.98 for the other models). As expected, the ERA-Interim land surface scheme produced even higher continental means than the CR method.

Overall, though the calibration-free CR have showed outstanding performance with the simple mathematical formulations, e.g., in the conterminous United States (Ma and Szilagyi, 2019; Kim et al., 2019b) and in China (Ma et al., 2019), it was unlikely to outperform the other models in the arid Australian continent. The CR \( ET_a \) estimates were considerably biased in wet coastal areas, their spatial coherence with \( ET_{wb} \) was weaker than the other \( ET_a \) products, and their variation of continental means was suppressed.
Figure 2: Distributions of the mean annual \( \text{ET}_a \) for 2002-2012 produced by the (a) water balance, (b) CR method, (c) GLEAM, (d) PT-JPL, (e) FluxCom, (f) AWRA-L, (g) Noah3.3, (h) CLSMF2.5, and (i) ERA-Interim.
Figure 3: (a) Comparison of the continental means of the ETa estimates for 2002-2012, and (b) the Taylor diagram comparing the standard deviation, the root mean square error, and the pattern correlation between the modeled mean annual ETa and ETwb. The whiskers indicate the two standard deviations of the continental means.

Figure 4: Interannual variations of the continental annual means for 1980-2019 estimated by the nine methods. Note that the AWRA-L, the Noah3.3, and the CLSMF2.5 data are given from 2000, while the PT-JPL data were produced for 2002-2016.

3.2 Evaluation of interannual variability and temporal trends at the grid scale

Figure 5 displays spatial patterns of the standard deviations of annual ETa for 2002-2012 from the water balance and the eight models. The ETwb was highly variable particularly in the northern and the eastern parts relative to other regions. The high ETa variability in the northern and the eastern parts of Australia was illustrated by Pan et al. (2020) for which state-of-the-art physical, machine-learning, and land surface models were compared together. The interannual variability of CR ETa product, however, had much weaker than ETwb particularly in the northern and the eastern coastlines. It was smaller than that
generated by the physical (GLEAM and JPL) and the land surface models (AWRL-A, Noah3.3, CLSMF2.5, and ERA-Interim). While the vast majority of models in Pan et al. (2020) suggested the largest interannual ET$_a$ in regions with annual precipitation between 700 and 1,000 mm a$^{-1}$, the calibration-free CR method was unable to pronounce such variations in (semi-)humid locations.

In the global-scale evaluation of Pan et al. (2020), land surface models pronounced higher ET$_a$ variability relative to physical and machine-learning models. Figure 5 provide a consistent indication that the annual ET$_a$ averages from AWRA-L, Noah3.3, CLSMF2.5, and ERA-Interim had interannual variability much higher than those from the PT-JPL and the machine-learning FluxCom. Although physically-based, the GLEAM showed the similar ET$_a$ variations to the land surface models. The machine-learning FluxCom pronounced the suppressed interannual variability across the continent, as did in Pan et al. (2020) and Ma et al. (2020).

The maps in Figure 6 are distributions of the median trends in annual ET$_a$ time series over 2002-2012. Given the transition from the weak El-Nino in 2002 to the strong La-Nina in 2010-2012 (Miralles et al., 2014b), steep upward trends (> 40 mm a$^{-2}$) in ET$_{wb}$ were found around the northeastern and the eastern parts of Australia. Relative to ET$_{wb}$, the CR ET$_a$ estimates gradually increased in the same region, and in the coastal areas, they rather declined unexpectedly. On the contrary, despite discrepancies, the ET$_a$ products from the GLEAM, the AWRA-L, the Noah3.3, and CLSMF2.5 well reflected the variations expected from changes in sea surface temperatures. The PT-JPL and the ERA-Interim provided smaller areas with the strong ET$_a$ trends. Although significant, the rising trends of the FluxCom were the smallest among the eight models with the unexpected declining trends in the eastern coast.
Figure 5: As in Figure 2, but for interannual variability for 2002-2012.
Figure 6: Distributions of the median trends in annual ETa time series for 2002-2012 given by the nine methods. The dots indicate the statistical significance at 5% level.
4 Discussion and perspectives

4.1 Performance of the CR method in Australia

In the continental-scale applications by Ma and Szilagyi (2019), Kim et al. (2019b), and Ma et al. (2019), the calibration-free CR formulation of Szilagyi et al. (2017) was superior to widely-used physical, machine learning, and land surface models. With the slight difference in calculation of T_w, here we applied the same approach for the continent smaller than the conterminous United States. Unexpectedly, the CR method performed worse than the chosen physical and land surface models, possibly because Australian land surfaces are mostly under (semi-)arid climates. In Szilagyi et al. (2017), the long-term sum of CR ET_a was often larger than that of precipitation in some locations in the western United States. Though the extensive irrigation for agriculture partly explains the unrealistically high ET_a in such an area (e.g., Szilagyi and Joza, 2018), questions still remain on the relatively poor performance of the CR method in (semi-)arid environments.

We here argue that the inferior performance of the CR method could be led by the parameter α_e=1.09 fixed across the large continent where climatic gradients are steep between dry inland and wet coastal areas. In Brutsaert et al. (2020), the Priestley-Taylor coefficient within a CR formulation is tightly related with climatological aridity. In other words, applying the constant α_e in every location could nullify the influence of climatological variation on the lower bound of ET_p. We hence checked the spatial variation of α_e optimal for the CR method by calibrating it against the long-term mean ET_w for 1991-2001 at each grid. Figure 7 displays the optimal α_e that minimizes the biases between the mean ET_w and CR ET_a, indicating that it tends to increase from coastal areas to western inland locations. In the western part, the calibrated α_e was often greater than the typical range of the Priestley-Taylor coefficient (1.1-1.32). The distribution of the optimal α_e was likely to reduce the positive biases in coastal locations and the underestimation in the western part produced by application of the constant α_e=1.09. When regenerating ET_a for 2002-2012 with the distributed α_e, the CR method became the best among the eight models in reproducing the temporal and spatial variations of mean ET_w and in the Taylor diagram (Figure 8). Note that the optimal α_e was found with the ET_w set separated from the new simulation.

The α_e distribution in Figure 7 provides a counteractive indication to Brutsaert et al. (2020) in which the parameter α_e within the CR of Brutsaert (2015) was calibrated against the eddy-covariance observations across the globe. The relationship between climatological aridity and α_e developed by Brutsaert et al. (2020) implicates the tendency of α_e exponentially decreasing with aridity. In contrast, Figure 7 indicates that wet regions have α_e values lower than in (semi-)arid inland locations. The central-eastern part receiving little precipitation has larger α_e values than the western part. The contradictory result from our work could be explained by the CR formulation from Brutsaert (2015). In the original CR derivation by Brutsaert (2015), ET_w was forced to become nil for ET_a = 0, posing an ill-defined assumption that R_a is always zero even when a desiccated surface is warm (Crago and Qualls, 2018; Szilagyi et al., 2017, Crago et al., 2016), and making the calibrated α_e oversensitively decline with aridity. Since Szilagyi et al. (2017) mended this problem by introducing the upper bound of ET_p (i.e., E_{pmax}), the calibrated α_e in Figure 7a would not hold the same sensitivity to aridity changes.
Instead, one could analytically relate the parameter $\alpha_e$ with climatic variables by equating the Penman and the Priestley-Taylor equations, because $ET_p$ and $ET_w$ must be equal under ample water conditions, yielding:

$$\alpha_e = 1 + \frac{\gamma}{\lambda} \frac{f_u VPD_{ws}}{R_n}$$  \hspace{1cm} (8)$$

where, $VPD_{ws}$ is the VPD of the atmosphere overpassing the hypothetical wet surface. Although $VPD_{ws}$ would be small owing to the interacting wet surface (Brutsaert and Stricker, 1979), Eq. (8) implies that the climatic variables, $R_n$, $\Delta_{ws}$, and $u_2$, could amplify the effects of $VPD_{ws}$ on $\alpha_e$. We conducted simple correlation analyses between the calibrated $\alpha_e$ values and the corresponding averages of $R_n$, $T_{avg}$ (i.e., the control of $\Delta_{ws}$), and $u_2$. The Pearson $r$ values of the $\alpha_e$ to the three variables were -0.56, 0.44, and 0.29, respectively (significant at 1% levels). The simple regression analyses, in addition, showed that the $R_n$, $T_{avg}$, and $u_2$ explain 32%, 19%, and 9% of the variation of the calibrated $\alpha_e$ values, respectively (significant at 1% levels). In other words, variation of $R_n$ plays a substantial role in determining the optimal $\alpha_e$ for the CR method, and it was found that locations with high $\alpha_e$ tend to have low $R_n$ (Figure 7b).

Nevertheless, the calibrated CR provided little improvements in reproducing the interannual variability and trends of $ET_w$. Despite the slightly increased interannual variability in central-northern areas, the new maps of interannual variability and trends (Figure 9) were still similar to the outcomes from the fixed $\alpha_e$=1.09. This might be attributable in part to vegetation dynamics neglected in the CR method. The Penman and Priestley-Taylor equations assume stationary land-surface parameters, and are unable to capture the plants’ behaviors to atmospheric conditions that play a considerable role in the precipitation partitioning (Jasechko, 2018). Modelling studies showed that the absence of surface responses to CO$_2$ fertilization has led offline hydrologic models to runoff projections contradictory to simulations of earth system models (e.g., Milly and Dunne, 2016; Swann et al., 2016; Roderick et al., 2015). Yang et al. (2019) mended this problem by incorporating a simple surface roughness formulation to the elevated CO$_2$ into the Penman-Monteith equation. Even though the CR method with the Penman
equation has worked well in Australia for the past decades (e.g., Crago and Quall, 2018), the prior studies suggest that surface responses to atmospheric changes could considerably affect temporal changes in $ET_p$, $ET_a$, and thus $ET_a$. This necessitates further refinements for the CR method to synthesize the surface behaviors explicitly under non-water-limiting conditions. It is worth noting that Australian carbon sink has enhanced during the 21st century even at increasing wildfire risks owing to the plants’ water-use efficiency and productivity increased by CO$_2$ fertilization (Kelly and Harrison, 2014).

In short, to capture the spatial variation of mean $ET_a$ in Australia, the CR method needs to consider the influence of climatic variables on the parameter $\alpha_e$. To regenerate the interannual variability and trends, the equations in the CR formulation are seemingly required incorporating dynamic surface parameters. In this case, the operational advantage of the CR method (i.e. no need of surface data) could disappear in return.

Figure 8: (a) interannual variation of the continental mean annual $ET_a$, (b) the distribution of mean annual $ET_a$ for 2002-2012 and (c) the Taylor diagram comparing the eight $ET_a$ products against $ET_{wb}$ when the CR method is calibrated.
Figure 9: The distributions of (a) interannual variability for 2002-2012 and (b) trends of annual ET$_a$ from the CR method with calibrated $\alpha$. The dots indicate the statistical significance at 5% level.

4.2 Intercomparison between ET$_a$ products

Since precipitation is the primary control of ET$_a$ in the dry continent, biases and errors in the GRUN and LORA runoff dataset are unlikely to induce large biases in the grid-scale water balance. As mentioned earlier, the ratio of ET$_a$ to precipitation is approximately 90% in Australia, suggesting that caveats in the GPCC precipitation are major error sources to ET$_{wb}$. Typically, errors in a grid precipitation product are introduced by: (i) the systematic measuring errors from evaporation out of rain gauges and aerodynamic effects, and (ii) the sampling errors from low gauging density. The GPCC precipitation takes an advanced correction and anomaly interpolation methods for reducing the systematic and the sampling errors via a very rigorous quality control framework (Schneider et al., 2014). The precipitation product has well closed the global water budget, becoming a reliable evaluation reference for other grid precipitation products (e.g., Sun et al., 2017). The quality of the GPCC data, hence, was unlikely a major concern.

Compared to ET$_{wb}$, however, the other ET$_a$ models are subject to diverse limitations. The remote-sensing physical models do not account for soil moisture dynamics playing a pivotal role in canopy conductance and bare soil evaporation in (semi-)arid regions (Pan et al., 2020). While the GLEAM takes soil moisture into account in the ET$_a$ synthesis, whereas the PT-JPL does not consider the soil moisture dynamics and underrates ET$_a$ in shrubs and deserts in the southern hemisphere (Miralles et al., 2016). Given that bare soil evaporation introduces the largest error to ET$_a$ estimates (Talsma et al., 2018), the PT-JPL needs any corrections for operational ET$_a$ monitoring in Australia.

On the other hand, the machine-learning FluxCom, which showed the worst performance in this work, has important caveats. Even though it acceptably simulates long-term averages of the surface energy fluxes, the FluxCom carbon fluxes are...
likely to have too small interannual variations in the energy fluxes (Jung et al., 2019). Recently, Ma et al. (2020) also emphasized the deficiency of the FluxCom in reproducing long-term ET$_a$ trends in the United States. Given that predictive performance of a machine-learning algorithm depends critically on training datasets (Yao et al., 2017), the machine learning ET$_a$ product needs to be further trained by any datasets describing the interannual behaviors.

Pan et al. (2020) showed that interannual variability of ET$_a$ products by 14 land surface models was dominantly controlled by precipitation in most of regions in the Southern Hemisphere. However, they also highlighted the dynamic root parameterization of the ORCHIDEE-MICT model (Guimberteau et al., 2018), which is distinguishable from the other models, suggesting that ET$_a$ changes in Australia could be less sensitive to precipitation changes than indicated by commonly-adopted land surface models. Hence, larger interannual variability than in ET$_{wb}$ could be an indication that land surface parameterization might be oversensitive to precipitation changes (e.g., the simulations in the eastern part by the AWRA-L and the CLSMF2.5).

Though it outperformed other models in streamflow generation (Frost et al., 2015), the AWRA-L needs corrections for the unexpected dry hotspots in inland areas. The two LIS land surface models, in addition, provided a consistent indication with the prior application for the Upper Blue Nile River (Jung et al., 2017). The CLSMF2.5 tends to provide higher ET$_a$ and lower streamflow than the Noah3.3, and it better represented the water budget in the sub-humid river basin. The overestimation in the ERA-Interim product was also found by Miralles et al. (2016) and Mueller et al. (2013). Sun et al. (2017) pointed out that the ERA-Interim often prescribed annual precipitation exceeding the GPCC P data.

5 Conclusions

In this work, we evaluated applicability of the calibration-free CR formulation in Australian land surfaces mostly under (semi-)arid climates. The terrestrial evapotranspiration (ET$_a$) produced by the CR method was compared with a bunch of ET$_a$ products from physical, machine-learning, and land surface models, and their spatial and temporal variations and decadal trends were evaluated against the estimates from water balance. While it could generate the ET$_a$ product strongly correlated with the water-balance estimates, the CR method seemed to introduce considerable biases when comparing to the other models. In Australia mostly under (semi-)arid climates, the approach proposed by Szilagyi et al. (2017) was unlikely to outperform typically-adopted physical, machine-learning, and land surface models, and thus necessitates better parameterization for improvement. We draw the following conclusions worth emphasizing:

(1) The optimal coefficient ($\alpha_e$) for the wet-environment evapotranspiration is unlikely constant. The $\alpha_e=1.09$ obtained from the calibration-free approach introduced positive biases in (semi-)humid coastal areas while underestimating in arid locations. When calibrating $\alpha_e$ each grid with the independent set of water-balance estimates, $\alpha_e$ seems to respond to climatic variations.

(2) Even with the calibrated $\alpha_e$, the CR method insufficiently captured the interannual variability and the decadal trends of the water-balance estimates at the grid scale. Since the latent heat flux is not only controlled by water stress but atmospheric conditions (e.g., CO$_2$ concentration), any formulation that captures land surface behaviors
under non-water-liming conditions would be necessary in quantification of the wet-environment and potential evapotranspiration.

(3) The evaluations of the physical, the machine-learning, and the land surface models provided a consistent implication with the prior global-scale studies. A remote-sensing physical model can better represent the surface energy balance by explicit consideration of soil moisture dynamics. The machine-learning depending largely on training datasets can suppress interannual variability and lead to overestimation in arid locations. ET_a products from land surface models could be more sensitive to precipitation variability than physical and machine-learning models.

### Author contributions

DK, MC, and JAC designed the study all together. DK simulated terrestrial evapotranspiration with the CR method and drafted the manuscript. JAC run the LIS land surface models and collected the other datasets for comparative evaluation. MC participated in discussion and review of the results and the manuscript.

### Competing interests

The authors declare no competing interests.

### Code availability

The R scripts for the CR method are available upon request from the leading author (daeha.kim@jbnu.ac.kr).

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Appendix: Calibration-free determination of $\alpha_e$ for the Australian continent.

In Szilagyi et al. (2017) and Ma et al. (2019), $\alpha_e$ values for ET$_w$ were determined by inserting the Priestley-Taylor equation into the Bowen ratio for a wet environment as:

$$\frac{R_n-ET_w}{ET_w} = \frac{1-\alpha_e}{\Delta_w} = \frac{\Delta_w}{\alpha_e \Delta_w + \gamma}$$  \hspace{1cm} (A1)

where, $\Delta_w$ is the slope of the saturation vapor pressure curve at the wet-environment air temperature ($T_w$) and the other variables have the same definitions in section 2.1. By rearranging Eq. (A1), $\alpha_e$ could be analytically obtained:

$$\alpha_e = \frac{[\Delta_w + \gamma][e_s(T_{ws})-e_a]}{\Delta_w[\gamma(T_{ws}-T_w)+e_s(T_{ws})-e_a]}$$  \hspace{1cm} (A2)

Szilagyi et al. (2017) identified local wet cells within a large region using sufficiently fine relative humidity (RH) and $T_{ws}$ data from Eq. (4a). The $\alpha_e$ values for wet cells are calculated with Eq. (A2) by inserting the measured air temperature into $T_w$, and are expected to fall within the theoretical limits of $[1, (\Delta_w + \gamma)/\Delta_w]$ (Priestley and Taylor, 1972).

In this work, the wet cells within the Australian continent were identified as locations satisfying the two conditions of $T_{ws} > T_{avg} + 3^\circ C$ and RH $> 90\%$. While Szilagyi et al. (2017) used $T_{ws} > T_{avg} + 2^\circ C$, we considered the fact that $T_{ws}$ estimates from Monteith (1981) is approximately $1^\circ C$ higher than those estimated by the implicit Bowen ratio (Szilagyi, 2014). The results showed that very few cells (less than 1% of the Australian continent) satisfied the given criteria and their $\alpha_e$ values from Eq. (A2) were within a very narrow range of $1.09 \pm 0.01$ (mean $\pm$ standard deviation). This calibration-free approach assumes that the mean of the $\alpha_e$ values is applicable for the entire region, thus assuming that a suitable $\alpha_e$ is spatially and temporally constant. More details are found in the Appendix B in Ma and Szilagyi (2019).