Nurse Staff Allocation in a Multi-stage Queuing System with Patients’ Feedback Flow for an Outpatient Department

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Received July, 2013

ABSTRACT

A general multi-stage queuing system model with patients’ feedback flow is developed to address the behavior of patients’ flow in an Outpatient Department (OD) in a hospital. The whole process includes registration, diagnosis, chemical examination, payment, and medicine-taking. Focusing on nurse resources, the formulas of performance indicators such as patient waiting times and nurse idle times are derived by using the system parameters. A mathematical programming model is developed to determine how many nurses should be allocated to each stage to minimize the total costs of patient waiting times and nurse idle times. The neighborhood search combined Simulated Annealing (NS-SA) is developed to solve the model, which is essentially a natural number decomposition problem. Numerical experiments are conducted to analyze the discipline of nurse allocation and the impact of patient arrival rates and the probability of patient’s feedback flow on the system costs. The research results will be helpful for hospital managers to make decisions on allocation of nurse staff in practice.

Keywords: Queuing; Nurse Staff Allocation; Healthcare; Simulated Annealing

1. Introduction

Over the years, hospital managers continually confront many challenges, such as providing better service quality, with less nurse staff and more patients. Especially, those conflicts are more severe in the out patient departments (OD)[1]. For example, there are 171,024 outpatients in a general hospital in Dalian, and 2,264,733 outpatients in a famous union hospital in Beijing, China in 2010. How to provide better service level with limited resources and increasing outpatients is a key problem in the hospital so that more and more researchers and practitioners begin to address it in recent years.

Health care service systems are essentially queuing systems. Queuing theory as an efficient tool has been used frequently to address the behavior of health-care service systems since Jackson network model was proposed in 1957[2-5]. Nurse staff allocation in multi-stage queuing system with patients’ feedback flow for OD is mainly concerned in this paper. Around of the queuing system in hospital Jlassi (2010) made a review on multiple customer types in Emergency Department(ED)[6]. According to the performance indicators such as patient waiting times, and the probability of nurse idle times in the multi-severs queuing systems, Abadi(2000)[7] and Balsamo made some analysis[8]. A three tandem queuing system was founded by El-Darzi (1998) in a hospital geriatric department[9]. Koizumi (2005) formulated a model of patient flows using a queuing network with blocking with finite waiting space and the feedback patients flow[10]. Carolina (2009) presented an analytic queuing network model which preserves the finite capacity of queues and used structural parameters to obtain the correlation between two stages[11]. The variation in patient flows is described by Kurt (2011) with the help of the work of [10,11]. However he paid no attention to the structure of the queuing networks and the patients flow-variability[12]. Some insights of patient flows just as the feedback patients flow in hospital are derived by Hall (2006), Helm (2011), Price (2011)[13-15].Focusing on the staffing allocation Ruger(2007) identified high-risk patients for triage and resource allocation in ED[16]. Mohamed(2009)made a simulation optimization model for an emergency department healthcare unit in Kuwait[17]. Navid(2012)set nurses staffing requirements for time dependent queuing network in ED with the square root method[18]. Kurt(2011)developed anew heu-
ristic for finite resource allocation in healthcare operations. But the feedback patients flow in queuing system isn’t considered in the above papers. The research on the analysis of the structure in OD with feedback patients and patients flow by routing probability is rarely known.

The data are collected for fitting the model parameters from Dalian Xinhua hospital in Liaoning province, China. Firstly, we characterize the patients’ medical treatment processes in OD and establish a general multi-stage feedback queuing system with feedback patients flow. The queuing model is formulated to address the behavior of patients flow starting from registration, diagnosis, chemical examination, payment, and medicine-taking. Focusing on the nurse resources, the formula of performance indicators such as patient waiting times, probability of nurse idle times are derived by the system parameters. A mathematical programming model is developed to determine how many nurses are allocated to each stage/division to minimize the total costs of patient waiting times and nurse idle times. The total cost of OD is summed of the patient’s waiting time cost and the healthcare staff idle time cost. The model is essentially a natural number decomposition problem, and thus a neighborhood search combined Simulated Annealing (NS-SA) is developed for solving it. Numerical experiments are conducted to analyze the discipline of nurse allocation and the impact of the patient arrival rates and the probability of feedback patient flow on system cost. Some insights are derived from numeric analysis at last. Our primary concern is the impact with the system performance indicators and the capacity of various stages. We assume that the nurses are in the broadest sense of the healthcare staff (nurse, medical equipment operator, cashier etc.).

This paper is structured as follows: section 2 presents the description of the queuing system model with feedback patients flow in OD. Medical treatment processes flowchart, mathematical formulations by analyzing steady states and the mathematical method to obtain performance indicators are introduced in this section. In section 3 a mathematical programming model is developed to determine how many nurses are allocated to each stage/division to minimize the total costs of patients waiting time and the nurse idle time. A neighborhood search combined Simulated Annealing (NS-SA) algorithm is developed. Section 4 presents numeric analysis of experiment results and Section 5 concludes the paper and provides the research direction in future.

2. Queuing System in OD

When a patient enters into an outpatient department, he should go to the registration station first, and then see doctor. If there is no question in the result after the doctor’s diagnosis, he will take the medicine after paying. Otherwise, he needs to make a serial examination process, e.g. CT, blood testing, and returns to see doctor after having testing results. The treatment flow chart in OD from patient registration to leaving is described as shown in Figure 1.

Without loss of generality, a general OD treatment process flowchart is simplified in Figure 2.

- The patients’ external arrival rate is a Poisson distribution with parameter \( \lambda \). All patients will be served sequentially with the rule FCFS (first come first service) before leaving the system. It is assumed there is an infinite buffer between any two stations and the system is steady-state.

- The network is a multi-stage queuing system with feedback patients flow where the four stages are M/M/n queuing model with capacity of stages \( N_i \) servers respectively. The patient arrival rate is a Poisson distribution with parameter \( \lambda_i \) before stage \( i \). The service rate in stage \( i \) is independent and aexponential distribution with parameter \( u_i \). The service time in examination stage is a general distribution with parameter \( u_5 \). The input patients flow is \( \lambda_5 \) and the output patients’ flow (re-enter station 2) is \( \lambda_6 \).

![Figure 1. OD medical treatment process flow chart.](image1)

![Figure 2. Simplified OD queuing system.](image2)
After seeing a doctor, the patient may have further examination with probability \( p_1 \), enter the 3rd stage with probability \( p_2 \) or quit the system with probability \( p_3 \). Then \( p_1 + p_2 + p_3 = 1 \).

- We note that the patients’ total waiting times is \( W \). The expected queue length is \( L_i \) at stage \( i \) respectively. The mean service intensity at stage \( i \) is \( \rho_i \). The queuing time before examination is \( W_D \) and the service intensity is \( \rho \). The probability that the system completely lose is \( \pi_{bo} \) and the probability that there are \( k \) servers are occupied is \( \pi_k \) at stage \( i \).

In the system, the input patient flow of the feedback flow is obtained from the routing probability and the external arrival rate \( \lambda \), then \( \lambda = p_1 \lambda \). In the equation, \( \rho = \frac{p_i \lambda}{u_5} < 1 \) is known as the service intensity at examination station. In M/G/1 queueing system, the busy period is \( p_c = \rho \frac{\lambda}{u_5} \) and the idle period is \( 1 - \rho \). In other words, the output patients’ flow is \( u_5 \) when the system is busy and the output patients’ flow is \( p_c \lambda \) when the system is idle. The equation of output patient can be obtained:

\[
\lambda = \rho \frac{\lambda}{u_5} + p_1 \lambda (1 - \rho) = p_1 \lambda (2 - \rho) \quad (1)
\]

The patients flow before the diagnosis station:

\[
\lambda = \lambda_0 = \lambda = p_1 \lambda (2 - \rho) \quad (2)
\]

The patients flow before the payment station:

\[
\lambda = \lambda = (1 - p_1 - p_3) + p_1 \lambda (2 - \rho) (1 - p_4) \quad (3)
\]

The patients flow before the medicine-taking station:

\[
\lambda = \lambda_0 \quad (4)
\]

The expected queue length at stage \( i \) is obtained by equations (1), (2), (3) and (4) in steady-state:

\[
L(N_i) = \left[ \sum_{n=1}^{N_i} \frac{\omega_n^N_i}{n!} + \frac{\omega_n^N_i}{(1 - \rho) N_i} \right]^{-1} \frac{\rho \omega_n^N_i}{(1 - \rho)^2 N_i!} \quad (5)
\]

where

\[
\omega = \lambda / u_5, p_i = \omega / N_i < 1 \quad (6)
\]

Equation (6) is essentially the stability condition for equation (5) hold in queuing theory. The expected waiting time to enter stage \( i \) at steady-state is obtained by equation:

\[
W(N_i) = L_i / \lambda = \left[ \sum_{n=1}^{N_i} \frac{\omega_n^N_i}{n!} + \frac{\omega_n^N_i}{(1 - \rho) N_i} \right]^{-1} \frac{\rho \omega_n^N_i}{(1 - \rho)^2 \lambda N_i!} \quad (7)
\]

The expected patients waiting time before examination:

\[
W_D = \frac{\rho}{2(1 - \rho) u_5} \quad (8)
\]

The patients total waiting time:

\[
W = \sum W(N_i) + p_d W_D \quad (9)
\]

The probability that the system completely lose at stage \( i \):

\[
\pi_{bo} = \left[ \sum_{k=0}^{N_i} \frac{(N_i \omega)^k}{k!} + \frac{(N_i \omega)^{N_i}}{N_i!(1 - \omega)} \right]^{-1} \quad (10)
\]

The probability that there are \( k \) servers are occupied at stage \( i \):

\[
\pi_k = \begin{cases} \frac{(N_i \omega)^k \pi_{bo}}{k!}, k = 1, 2, ..., N_i - 1 \\ \frac{N_i^k \omega^k \pi_{bo}}{N_i!}, k = N_i, N_i + 1, ..., \end{cases} \quad (11)
\]

Then the expression of the main performance indicators in OD has been obtained.

### 3. The Nurses Allocation Model

The cost of OD is usually described by the patients waiting time cost and health care staff idle time cost [19]. A mathematical programming model is developed to determine how many nurses are allocated to each stage/division to minimize the total costs of patients’ waiting time and the nurse idle time. We assumed the number of nurses \( N \) in OD is fixed, and the nurses are multi-skilled. Jobs in different stations can be arbitrarily assigned. In other words, all nurses can be allocated to all kinds of job. We note the cost of OD is \( C \), the ratio between nurse’s idle time cost and patient’s waiting time cost \( \alpha \) . Unit cost expressed in minutes. We also assume that the cycle is \( T \). By formula (9), (10) and (11), a cost model based on nurses allocation in out patient departments (CMNAOD) is described:

\[
T \left( \sum N_i \omega_i W(N_i)^{\gamma} + \lambda \alpha p_d W_D + \min \left\{ \sum_{k=1}^{N_i} \frac{(N_i \omega)^k}{k!} \pi_{bo} + \sum N_i u_i \pi_{bo} \right\} \right) \quad (12)
\]

s.t \( N_i \geq 1, N_i \text{ is integer} \quad (13) \)

\[
\omega_i = \lambda / u_5, \rho_i = \omega / N_i < 1 \quad (14) \]

\[
\alpha < 1 \quad (15)
\]

The number of nurses is fixed by constraint equation (12). Equation (14) is essentially the stability condition in the queuing system. According to the relevant literatures,
the nurse’s idle time cost is generally bigger than the patient’s waiting time cost in (15).

3.1. A Neighborhood Search combined Simulated Annealing (NS-SA) Algorithm

The optimal solution of CMNAOD is determined by nurse staff allocation which is essentially a natural number decomposition problem with constraints. With the increasing of \( N \), the number of feasible solution becomes very larger. For example, when the \( N = 10 \), the number of nurses allocation is 84 and \( N = 100 \), the number of nurses allocation is 156849. With the increasing of \( N \), how to find the optimal solution by enumeration becomes very difficult. Thus a neighborhood search combined Simulated Annealing (NS-SA) algorithm is developed.

NS-SA as a meta-heuristic with stochastic neighborhood search has successfully solved many large-scale combinatorial optimization problems [20-22]. CMNAOD model is a nonlinear integer programming model, which is essentially a combinatorial optimization problem based on the decomposition of natural numbers. According to the problem character, NS-SA is qualified to solve the problem very well.

To accomplish NS-SA, several core technical issues should be solved such as the initial solution generation, the definition of neighborhood and the cooling schedule. We introduce these critical operations in our NS-SA algorithm in details as followings.

3.1.1. Initial Solution Generators

The integer coding method is adopted in the algorithm. An example solution can be coded as \( X=[N_1,N_2,N_3,N_4] \). Each variable \( N(i=1,2,3,4) \) indicates the number of nurses assigned to system node \( i \).

We develop a heuristic approach to generate a good initial solution. The basic idea is described as followings:

1) Calculate the minimum number of nurses \( min(N_i) \) assigned to each system node according to constraints (12), (13) and (14). Let \( N_i \) is the maximum number of nurses assigned to node 1 by calculating

\[
\max(N_i) = N - \sum_{i=2}^{4} \min(N_i),
\]

and the rest nodes are assigned with the minimum number of nurses. Therefore, a solution can be obtained as \( X_0 \). Let the number of iterations to be \( j = 1 \);

2) Let \( N_i = N_i - 1 \), and calculate the corresponding objective value by adding 1 to \( N_2 \), \( N_3 \), \( N_4 \) respectively. Save the best solution as \( X_j \), whose objective value is the minimum one;

3) If \( j = \max(N_i) - \min(N_i) \), turn to 4); else let \( j = j + 1 \), and turn to 2);

Select a best solution from the solutions obtained above, whose objective value is the minimum one. Let the best solution is the initial solution \( X^* \).

3.1.2. Neighborhood Generation Strategy

The neighborhood generation is performed on the variable set \( X=[N_1,N_2,N_3,N_4] \). Two random numbers are generated to choose the items which are replaced to generate the neighborhood of the variable set (i.e., one item plus 1, the other minus 1). Specific operations are described as follows: select one item randomly, and judge whether \( N_i \) is equal to \( \min(N_i) \) or not. If \( N_i \) is not equal to \( \min(N_i) \), \( N_i \) decreases 1; otherwise, \( N_i \) adds 1. Then, randomly select another item \( N_j \), and \( j \) is not equal to \( i \). If \( N_j \) adds 1 and \( N_j \) is not equal to \( \min(N_j) \), \( N_j \) decreases 1. If \( N_j \) decreases 1, \( N_j \) adds 1. Otherwise, reselect \( j \).

The metropolis rule is adopted in the algorithm. The neighborhood solution is accepted if the objective value decreases; otherwise, the neighborhood solution is accepted based on the following acceptance probability:

\[
\min[1, \exp(-\Delta f / t_j)] > \text{random}(0,1)
\]

3.1.3. Cooling Schedule

The temperature is decreased according to the Equation

\[
t_{k+1} = t_k \cdot p, \quad \text{where} \quad p \quad \text{is the cooling rate and its value is defined between 0.95 and 0.99.}
\]

4. Numeric Analysis

In order to obtain the value of performance indicators, we must obtain the series of parameters including the external arrival rate of patients \( \lambda \), the patients routing probability \( p_i \), the per-server service rate \( u_i \), the number of servers \( N_i \). \( N_i \) is obtained by the direct observation and \( p_i \) is obtained by ageneral statistical method from data. We use a method of parameter estimation to obtain the values of \( \lambda \) and \( u_i \). The values of the parameters are derived from the maximum likelihood estimation. The Chi-square goodness of fit tests is performed to evaluate the fit of the models. The 171,024 observations from January 1, 2010 to June 30, 2011 are obtained from Dalian XinHua hospital in China. The value of the external arrival rate is 1.892. The same calculation process of the service rate is done in a similar way. The values of the model parameters are presented as shown in Table 1.

The NS-SA algorithm is implemented by using C# programming language in Visual Studio 2008. The optimal solution of nurse staff allocation is: \( N_1=9, N_2=12, N_3=5, N_4=4 \). The cost of OD is 722.916min with the nurse idle time costs and the patient waiting time costs.

4.1. \( \lambda \) for the Impact of System Values

The patient arrival rates varying from (0.1, 1.892) with other parameters are fixed. The variation of the costs of
OD, the nurse idle time costs and the patient waiting time costs are shown in Figure 3. From Figure 3, some insights are obtained as following.

a) With the increasing patient arrival rate, the patients excepted waiting time cost in the system is significantly increasing.

b) With the increasing patient arrival rate, the nurse idle time cost in the system is significantly decreasing. The optimal solution of the costs of OD is $\lambda = 1.3$ when $N_1=8$, $N_2=12$, $N_3=6$, $N_4=4$.

4.2. $p_1$ for the Impact of System Values

With the patient routing probability input examination station $p_1$ varying from (0.1,1.892) and other parameters are fixed, so the changes of the costs of OD, the nurse idle time costs and the patient waiting time costs are shown in Figure 4. From Figure 4, some insights are obtained as following.

![Figure 3. $\lambda$ for the impact of system values.](image)

![Figure 4. $p_1$ for the impact of system values.](image)

**Table 1. Parameters and description.**

| parameter | description | values  | $i$  |
|-----------|-------------|---------|------|
| $p_1$     | routing probability | 0.8149  | 1    |
|           |             | 0.1351  | 2    |
|           |             | 0.05    | 3    |
|           |             | 0.05    | 4    |
| $\lambda$ | external arrival rate | 1.892   |      |
| $H_i$     | per-server service rate | 0.5137  | 1    |
|           |             | 0.3543  | 2    |
|           |             | 0.5747  | 3    |
|           |             | 0.7748  | 4    |
|           |             | 0.16    | 5    |
| $T$       | the cycle   | 240min  |      |
| $N$       | the total servers | 30      |      |
| $\alpha$  | the ratio between nurse’ idle time cost and patient’s waiting time cost | 0.2     |      |

a) With the increasing patient routing probability input examination station, the patient waiting time costs in the system is significantly increasing before $p_1 = 0.45$. But after $p_1 = 0.45$, the values of the patient waiting time costs are stable. The main reason for this phenomenon is that the examination station is a regulator to our queuing systems[23].

b) With the increasing patient routing probability input examination station, the nurse idle time costs in the system is significantly decreasing before $p_1 = 0.45$. But after $p_1 = 0.45$, the values of the nurse idle time costs become stable with the same reason as above.

5. Conclusions

In this paper, a general multi-stage queuing system model with feedback patient flow about OD is addressed. A mathematical programming model is developed with nurse staff allocation and a NS-S A algorithm is developed. Numeric analysis is done by patient arrival rates and patient routing probability input examination station. Some insights are obtained by the numeric analysis. The optimal routing policy and queuing rule in the scenarios of the feedback patient flow returning to diagnosis is worthy of addressing in the future.

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