IDENTIFICATION OF TARGET SYSTEM OPERATIONS. DETERMINATION OF THE VALUE OF THE COMPLEX COSTS OF THE TARGET OPERATION

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1. Introduction

Determination of the time of the actual completion of the target operation [1] outlines the time range of the study, in which data processing of the operation is carried out. This processing is performed in order to obtain parameters that allow to identify the investigated operation.

One of such basic traditional indicators are costs of operation. The concept of “costs” is rather a tribute to the influence of the accounting terms. This concept, for lack of a suitable alternative, is widely used not only by economists, but also specialists in technical systems, as well as cyberneticists. For example, consumption, the need for raw materials and costs of operation are generally considered synonymous.

However, when it comes to management and optimization, a popular approach is the minimization of energy costs. The question that the minimization of the energy product consumption leads to a change in operation time and, as a rule, to its significant delaying remains «behind the scenes».

In this sense, the task of developing a fundamentally different, cybernetic indicator, which allows to take into account the influence of the change in the energy product consumption, duration of binding raw products of the operation on the operation time and effectiveness is interesting. Since the operation is carried out in order to obtain the result, but not with the purpose of saving energy products.

2. Analysis of the literature data and problem statement

Cost reduction was and is today a very topical issue [2]. Costs are controlled [3], optimized, reduced [4] and saved [5].

At the same time, it is clear that costs or expenses is not an independent indicator of the target operation, since two operations, that have the same costs and different duration, have different efficiency, and costs do not indicate this fact without the use of additional indicators.

A similar problem occurs if two operations with similar costs have different values added (profit). In this case, profitability indicator, based on the costs is introduced, but the time factor does not allow to consider this indicator as an independent pointer to a more efficient operation. More profitable, but durable operation may be less effective in relation to the less profitable and less durable operation.

The above is true for problems with the Pareto optimum [6].
In such circumstances, obtaining practically useful result is usually achieved using mathematical modeling methods in searching for the best solution [7].

### 3. Goal and objectives

The goal is to develop a fundamentally new indicator of the target operation "complex costs (resource intensity)" and obtain an expression for numerical and analytical determination of this new cybernetic category.

For this purpose, the following tasks were solved:
1. Determination of the value of resource consumption at the time of the actual completion of the target operation;
2. Determination of the value of resource return at the time of the actual completion of the target operation;
3. Determination of losses of management in the form of a closed thread of mismatch of resource consumption and resource return thread on the interval from the start of the operation until the actual completion;
4. Determination of the complex losses of management (resource intensity of the operation) in the form of the integral value of losses of management at the time of the actual completion of the target operation.

### 4. Complex costs of the target operation

As was shown [1], any effective target operation begins with the resource consumption process, passing in the resource return process. The resource consumption process can be displayed as a closed thread of tight resources, and resource return process - in the form of the target thread (Fig. 1).

The time of the actual completion of the operation (MFZO) determines the time of compensation of the resource consumption thread by the resource return thread [8]. However, this compensation is carried out only in magnitude. In time, it can be clearly seen when considering the thread of tight resources vbe(t) and the resulting thread ide(t), these threads are spread over and, consequently, at the MFZO there are irreparable system losses of management.

These losses can be defined as the value of the integral function of mismatch at the MFZO. That is, system losses of management as a closed thread of mismatch of resource consumption thread vbe(t) and integral function of the resulting thread ide(t) on the interval from the start of the operation until the actual completion (Fig. 1).

Equivalent approach is to determine the losses of management by mismatching the integral value of losses of management thread vre(t) and integral function of the resource return thread vpe(t) on the interval from the start of the operation until the actual completion.

Let us define the function of system losses of management on an example of the study of a simple operation, set in the form of a tuple \((RE = -2, t = 2; PE = 4, t = 8)\).

1. We determine the MFZO from the expression \(t_a = \frac{PE \cdot t_p - |RE| \cdot t_s}{PE - |RE|} = 20 \text{ s.}\)

2. We introduce an auxiliary variable \(v\) and denote it as \(v \in [t_a; t_a^*].\)

3. We build a model of the operation on the interval \([v_a = t_a; v_s = t_s]\) (Fig. 2).

\[
\text{ire}(v) = \int_{v_a}^{v_s} \text{re}(v) \, dv, \quad \text{ipe}(v) = \int_{v_a}^{v_s} \text{pe}(v) \, dv.
\]

4. We form the integral function of resource consumption and resource return threads on the interval \([v_a = t_a; v_s = t_s]\) (Fig. 2).

\[
\text{vre}(v) = \int_{v_a}^{v_s} \text{re}(v) \, dv, \quad \text{vpe}(v) = \int_{v_a}^{v_s} \text{pe}(v) \, dv.
\]

5. We define losses of management as a closed thread of mismatch on the interval from the start of the operation until the actual completion (Fig. 3).

\[
\text{dif}(v) = \int_{v_a}^{v_s} \text{re}(v) \, dv - \int_{v_a}^{v_s} \text{pe}(v) \, dv.
\]

6. We determine the integral function of losses of management (Fig. 4)
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\[ r(v) = \left. \left[ \frac{\int_{v}^{v_1} ir(v) \, dv}{v} \right] \right|_{v_1}^{v_0} - \left. \left[ \frac{\int_{v}^{v_0} pe(v) \, dv}{v} \right] \right|_{v_1}^{v_0}. \]

Fig. 3 Uncompensated losses of management in the form of a closed thread \( d(v) \)

Fig. 4 The function of change of complex losses of management (resource intensity) of the target operation

The value of the resource intensity of the target operation is numerically equal to the ratio of the product of cost estimates of the module of the value of the input product, the value of the output product and the square of the difference between the time of their registration to the doubled value of the difference between the cost estimates of the module of the value of the input and output products.

As can be seen, the results obtained using a numerical method correspond to the result obtained using the analytical expression for determining resource intensity.

Let us consider the way the resource intensity responds to changes in the parameters of target operations in those cases where the result is guaranteed to be predictable.

Each operation of a set has the cost estimate of input products of the operation (\( RE \) – costs), cost estimate of output products of the operation (\( PE \) ) and the operation time (\( t_{op} \)). Also, resource intensity (\( R \)), which is seen in the diagrams together with costs is calculated for each operation.

5. Analytical determination of complex costs (resource intensity) of a simple target operation

Since the resource intensity of the simple target operation, based on the geometric interpretation of losses of management, is the area of triangle ABC (Fig. 2), it can be defined as the difference of triangles ABD and CBD.

By substituting scalar values \( ire' \left[ t_s \right] t_s \) and \( ip'e' \left[ t_s \right] t_s \) for the functions \( ire' \left[ t \right] t \) and \( ip'e' \left[ t \right] t \) we obtain the expressions

\[ 0 = ire' \left[ t_s \right] t_s - ire' \left[ t_s \right] t_s + C, \]
\[ 0 = ip'e' \left[ t_s \right] t_s - ip'e' \left[ t_s \right] t_s + C. \]

By presenting them in the form of a system of equations and solving with respect to \( C \), we obtain an expression for determining the height \( BD \)

\[ BD = \frac{ire' \left[ t_s \right] t_s - ire' \left[ t_s \right] t_s}{ip'e' \left[ t_s \right] t_s - ip'e' \left[ t_s \right] t_s}. \]

Since we have defined the resource intensity of the simple operation as the difference of the right triangles, the expression for determining it will have the form of

\[ R = \frac{1}{2} \left( t_s - t_p \right) BD - \frac{1}{2} \left( t_s - t_p \right) BD. \]

By substituting its value for \( BD \) from the expression after the corresponding transformations, we obtain

\[ R = \frac{ip'e' \left[ t_s \right] \left[ t_s \right] \left( t_r - t_p \right)^2}{2 \left( ip'e' \left[ t_s \right] - ire' \left[ t_s \right] \right)}. \]

Given that for simple operations \( ip'e' \left[ t_s \right] \) is numerically equal to the value \( PE \), and \( ire' \left[ t_s \right] \) is numerically equal to the value \( RE \), to determine the numerical value of the resource intensity we can use the expression, which uses the values of the registration signals and moments of their formation

\[ R = \frac{PE \cdot RE \left( t_r - t_p \right)^2}{2 \left( PE - RE \right)}. \]

For example, for the considered operation (Fig. 1), we obtain

\[ R = \frac{PE \cdot RE \left( t_r - t_p \right)^2}{2 \left( PE - RE \right)} = \frac{3 \cdot 2.36}{2} = 108 \text{ CTT}. \]

The value of the resource intensity of the focused operation is numerically equal to the ratio of the product of cost estimates of the module of the value of the input product, the value of the output product and the square of the difference between the time of their registration to the doubled value of the difference between the cost estimates of the module of the value of the input and output products.

As can be seen, the results obtained using a numerical method correspond to the result obtained using the analytical expression for determining resource intensity.

Let us consider the way the resource intensity responds to changes in the parameters of target operations in those cases where the result is guaranteed to be predictable.

Each operation of a set has the cost estimate of input products of the operation (\( RE \) – costs), cost estimate of output products of the operation (\( PE \) ) and the operation time (\( t_{op} \)). Also, resource intensity (\( R \)), which is seen in the diagrams together with costs is calculated for each operation.
In the first set of operations, values \(RE\) and \(PE\) do not change, and the operation time \(T_o\) changes. Obviously, the longer the operation time (at fixed \(RE\) and \(PE\)), the longer the input products of the operation \(RE\) are bound by technological processes and the higher the resource intensity.

Calculation of the resource intensity for the first set of operations (Table 1) confirms this assumption (Fig. 5).

| Set of operations 1 | Set of operations 2 | Set of operations 3 |
|--------------------|--------------------|--------------------|
| \(N\) | \(RE\) | \(PE\) | \(T\) | \(R\) | \(N\) | \(RE\) | \(PE\) | \(T\) | \(R\) | \(N\) | \(RE\) | \(PE\) | \(T\) | \(R\) |
| 1 | 2 | 3 | 1 | 3 | 1 | 2 | 3 | 27 | 1 | 2 | 2,5 | 3 | 45 |
| 2 | 2 | 3 | 2 | 12 | 2 | 2,1 | 3 | 31,5 | 2 | 2 | 2,6 | 3 | 39 |
| 3 | 2 | 3 | 3 | 27 | 3 | 2,2 | 3 | 37,13 | 3 | 2 | 2,7 | 3 | 34,71 |
| 4 | 2 | 3 | 4 | 88 | 4 | 2,3 | 3 | 44,36 | 4 | 2 | 2,8 | 3 | 31,5 |
| 5 | 2 | 3 | 5 | 75 | 5 | 2,4 | 3 | 54 | 5 | 2 | 2,9 | 3 | 29 |
| 6 | 2 | 3 | 6 | 108 | 6 | 2,5 | 3 | 67,5 | 6 | 2 | 3 | 3 | 27 |
| 7 | 2 | 3 | 7 | 147 | 7 | 2,6 | 3 | 87,75 | 7 | 2 | 3,1 | 3 | 25,36 |

The second set of operations (Table 1) is characterized by the fact that, from operation to operation, the cost estimate of input products of the operation \(RE\) increases and the cost estimate of output products of the operation \(PE\) and the operation time \(T_o\) do not change. In this case, with an increase in the cost estimate of input products of the operation (costs \(RE\)), at constant \(PE\) and \(T_o\) resource intensity of the operation should increase. Calculation of the resource intensity for the second set of operations (see Table) confirms this assumption (Fig. 6).

The third set of operations (Table 1) is characterized by the fact that, from operation to operation, the cost estimate of output products of the operation \(PE\) increases and the cost estimate of input products of the operation \(RE\) and the operation time \(T_o\) do not change. Here, the change of the cost estimate of output products of the operation towards an increase speeds up the compensation of the resource consumption of the operation, and resource intensity must, in this case, decrease. Calculation of the resource intensity for the third set of operations (Table 1) confirms this assumption as well (Fig. 7).

In conclusion, let us consider the cycle of operations with minimum costs in the process of the proportional change of the operation time (Table 2).

| \(N\) | \(RE\) | \(PE\) | \(T\) | \(R\) | \(Prof\) |
|------|------|------|------|------|-------|
| 1    | 2    | 2,5  | 1    | 5    | 575,00 |
| 2    | 1,894| 2,5  | 1,05 | 4,31 | 663,71 |
| 3    | 1,824| 2,5  | 1,1  | 4,08 | 706,73 |
| 4    | 1,772| 2,5  | 1,15 | 4,02 | 728,00 |
| 5    | 1,75  | 2,5  | 1,2  | 4,2  | 718,75 |
| 6    | 1,738| 2,5  | 1,25 | 4,45 | 701,04 |
| 7    | 1,759| 2,5  | 1,3  | 5,01 | 655,50 |
| 8    | 1,791| 2,5  | 1,35 | 5,75 | 603,96 |
| 9    | 1,837| 2,5  | 1,4  | 6,79 | 544,61 |
| 10   | 1,913| 2,5  | 1,45 | 8,56 | 465,55 |
| 11   | 2    | 2,5  | 1,5  | 11,25 | 383,33 |

Calculation of resource intensity shows that its minimum does not match the minimum costs (Fig. 8).

Let us analyze the differences among the operations, indicated by the minimum costs (operation N6) and a minimum of resource intensity (operation N4).
Fig. 8. Resource intensity of the target operation depending on the change in costs and operation time

Thousand N4 type operations, carried out in the cycle lasts for $T = T_{op} \times 1000 = 1150$ hours. During this time, the operation generates the value added (profit) $Prof_4 = 1150 \times (PE - RE) = 1150 \times (2.5 - 1.772) = 728$ monetary units.

During the same time, the N6 type operation will be performed $I = 1150 / 1.25 = 920$ times. In this case, the N6 type operation generates the value added (profit) $Prof_6 = 920 \times (PE - RE) = 920 \times (2.5 - 1.738) = 701.04$ monetary units.

Thus, the target product $Prof_4$ exceeds the target product $Prof_6$ by 27 monetary units in absolute terms.

Carrying out these calculations for all operations of the set shows that the minimum resource intensity indicates the maximum generated target product (profit) (Fig. 9).

As can be seen from the Fig. 9, a change in resource intensity of the target operation is the mirror image of the function of the value added. Consequently, the maximum efficiency of a set of operations corresponds to the operation with minimum resource intensity.

8. Conclusions

The paper gives a new insight into the resource intensity of the target operation, which is its most important indicator. It was found that the concept of resource intensity of the target operation is based on such core categories as resource consumption of the operation (consumption of input products of the operation in time in comparable values) and resource return of the operation (generation of output products of the operation in time in comparable values).

Reliance on the functions of resource consumption and resource return, from the start of the target operation until the actual completion has allowed to quantify the value of its resource intensity.

Using the model of simple target operation has allowed to obtain an analytical expression of the resource intensity for the operations, in the study of which distributed parameters of registration functions of input and output products of the operation can be neglected.

Using mathematical modeling methods it was revealed that in the case of a fixed value of expert (cost) estimate of output products of the operation, minimum resource intensity of the target operation indicates the maximum efficiency operation with respect to the target product of the operation.

Using the developed indicator in search optimization systems allows to maximize financial result by increasing the amount of the value added by 5–25%.

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На основі теорії реологічних переходів виконані дослідження технологічних процесів. Показано, що такі процеси можна описати інтегральними імпульсними дельта-функціями Дірака. Приведені аналітичні рівняння, за якими можна розраховувати екстремалі технологічного процесу. Це дозволяє забезпечити максимальну ефективність технологічного процесу при мінімум енергетичних та матеріальних затрат.

Ключові слова: технологія, контроль, управління, перенесення, реологія, переход, дифузія, конвекція, екстремум, оптимізація.

1. Вступ

Технологічні процеси (ТП) хімічних, нафтохімічних, нафтопереробних, теплоенергетичних, фармацевтичних, харчових та інших виробництв відносяться до складних взаємопов’язаних багатопараметричних об’єктів контролю та управління з багатьма вхідними, вихідними та впливовими параметрами. Як правило, такі об’єкти описуються нелінійними диференціальними рівняннями перенесення енергії, маси та кількості руху. У зв’язку з тим, що методів розв’язку нелінійних інтегро-диференціальних рівнянь практично немає, то їх спрощують, приводять до рівнянь переносу, які визначають процеси передачі енергії, маси та кількості руху. У зв’язку з цим, методам розв’язання