A 2-3 mm high-resolution molecular line survey towards the centre of the nearby spiral galaxy NGC 6946*

Cosima Eibensteiner1,2,3, ⋆, Ashley T. Barnes1, Frank Bigiel1, Eva Schinnerer2, Daizhong Liu3, David S. Meier4, Antonio Usero3, Adam K. Leroy6, Erik Rosolowsky7, Johannes Puschnig1, Ilin Lazar5, Jérôme Pety9,10, Laura A. Lopez6, Eric Emsellem11,12, Ivana Bešlić1, Miguel Querejeta5, Eric J. Murphy13, Jakob den Brok1, Andreas Schruba3, Mélanie Chevance14, Simon C. O. Glover15, Yu Gao14, Kathryn Grasha16, Hamid Hassani7, Jonathan D. Henshaw2, María J. Jiménez-Donaire5, Ralf S. Klessen15,17, J. M. Diederik Kruisjens14, Hsi-An Pan19, Toshiki Saito2, Mattia C. Sormani15, Yu-Hsuan Teng20, and Thomas G. Williams2

(Affiliations can be found after the references)

Received 09 November 2021 / Accepted 20 December 2021

ABSTRACT

The complex physical, kinematic, and chemical properties of galaxy centres make them interesting environments to examine with molecular line emission. We present new 2–4″ (~75–150 pc at 7.7 Mpc) observations at 2 and 3 mm covering the central 50″ (~1.9 kpc) of the nearby double-barred spiral galaxy NGC 6946 obtained with the IRAM Plateau de Bure Interferometer. We detect spectral lines from ten molecules: CO, HCN, HCO+\(^+\), HNC, CS, HC3N, N2H+, C2H, CH3OH, and H2CO. We complemented these with published 1mm CO observations and 33 GHz continuum observations to explore the star formation rate surface density \(\Sigma_{\text{SFR}}\) on 150 pc scales. In this paper, we analyse regions associated with the inner bar of NGC 6946 – the nuclear region (NUC), the northern (NBE), and southern inner bar end (SBE) and we focus on short-spacing corrected bulk (CO) and dense gas tracers (HCN, HCO+, and HNC). We find that HCO+ correlates best with \(\Sigma_{\text{SFR}}\), but the dense gas fraction \(f_{\text{dense}}\) and star formation efficiency of the dense gas \(\text{SFE}_{\text{dense}}\) fits show different behaviours than expected from large-scale disc observations. The SBE has a higher \(\Sigma_{\text{SFR}}\), \(f_{\text{dense}}\), and shocked gas fraction than the NBE. We examine line ratio diagnostics and find a higher CO (2–1)/CO (1–0) ratio towards NBE than for the NUC. Moreover, comparison with existing extragalactic datasets suggests that using the HCN/HNC ratio to probe kinetic temperatures is not suitable on kiloparsec and sub-kiloparsec scales in extragalactic regions. Lastly, our study shows that the HCO+\(^+\)/HCN ratio might not be a unique indicator to diagnose AGN activity in galaxies.

Key words. galaxies: ISM – ISM: molecules – Galaxies: individual: NGC6946

1. Introduction

The study of star-forming regions within galaxy centres is of particular interest, as the extreme conditions within these regions are thought to greatly influence their host giant molecular cloud (GMC) populations, and, thus, the stellar populations that they may form. For example, the inner few kiloparsecs of galaxies typically have higher average gas and stellar densities, gas temperatures, levels of turbulence and magnetic field strengths relative to their discs. All of these characteristics have direct implications for the physical, dynamical and chemical properties of the star-forming ‘dense’ molecular gas within systems (see e.g. McKee & Ostriker 2007; Lada et al. 2010, 2012; Longmore et al. 2013; Klessen & Glover 2016).

Molecular gas is denser in centres than is typically inferred within disc star-forming regions; the cause of this is strong compressive tidal forces, frequent molecular cloud interactions, short dynamical timescales, constant feeding of material via, for example, bars (e.g. Schinnerer et al. 2006; Schinnerer et al. 2007), and feedback from both young and old stars (e.g. Krumholz et al. 2019; Chevance et al. 2020a,b; Barnes et al. 2020b) along with energetic phenomena within the galaxy centres (e.g. AGN; Combes et al. 2013; Querejeta et al. 2015) and this should favour star formation. However, it is seen both within the Milky Way (e.g. Krumholz et al. 2014; Barnes et al. 2017) and inferred at centres of nearby galaxies (e.g. Gallagher et al. 2018b; Jiménez-Donaire et al. 2019) that the gas over-density required to form stars is also higher. Averaged over the galaxy population (and thereby presumably over episodic variations, e.g. Krumholz et al., 2017), centres show an apparent deficit of star formation despite their large quantities of dense molecular gas (e.g. Bigiel et al. 2015; Usero et al. 2015; Jiménez-Donaire et al. 2019 among others). For a complete understanding of star formation, the study of these complex environments present in galaxy centres is crucial.

Observations and simulations of a Milky Way-like galaxy suggest that large-scale bars (a few kiloparsecs) could be responsible for a molecular gas mass build-up in the central few hundred parsecs (e.g. Diaz-Garcia et al. 2020 and Renaud et al. 2015; Emsellem et al. 2015; Sormani & Barnes 2019; Sormani et al. 2020). The overlap between the end of those large-scale bars and the spiral arms are – in addition to the centre – active star-forming regions coupled with enhanced dense gas, for ex-
ample the bar ends of NGC 3627 (Beuther et al. 2017; Bešlić et al. 2021). Secondary small-scale bars (a few hundred parsecs) of double barred galaxies (e.g. Erwin 2011) were intensively studied through photometric analysis (e.g. Méndez-Abreu et al. 2019; de Lorenzo-Cáceres et al. 2020). However, secondary small-scale bars (we refer to them as ‘inner bar’ in this work) have been hardly observed with emission from multiple rotational molecular line transitions. This leads us to question if we would find also enhanced molecular line emission (indicating what have been hardly observed with emission from multiple rota-

tional molecular line transitions. This leads us to question if we would find also enhanced molecular line emission (indicating a small-scale bar (we refer to them as ‘inner bar’ in this work), suggest the presence of large amounts of ‘dense’ molecular gas (Mauersberger et al. 1989; Mauersberger & Henkel 1989, 1991; Nguyen et al. 1992; Solomon et al. 1992; Helfer & Blitz 1993). More recently, higher angular resolution observations have allowed the study of dense gas content of individual centres of galaxies on sub-kiloparsec scales (e.g. Schinnerer et al. 2007; Pan et al. 2015 and Tan et al. 2018 for NGC 6946; Martín et al. 2015 for NGC 253; Murphy et al. 2015 for NGC 3627; Salek et al. 2018 for NGC 1808; Querejeta et al. 2019 for M 51; Benis & Wilson 2019 for NGC 4038 and NGC 4039; Callanan et al. 2021 for M 83).

Galaxy centres also have a rich and diverse chemistry that could be used to probe the environmental conditions of gas beyond just the density (e.g. Morris & Serabyn 1996; Belloche et al. 2013; Rathborne et al. 2015; Barnes et al. 2019 and Petkova et al. 2021 for the Milky Way; Meier & Turner 2005 for IC 342; Meier & Turner 2012 for Maffei 2; Aladro et al. 2013 for NGC 1068; Meier et al. 2015; Leroy et al. 2018; Krieger et al. 2020 and Holdship et al. 2021 for NGC 253; Martín et al. 2015 for NGC 1097; Henkel et al. 2018 for NGC 4945). These studies used molecular line ratio diagnostics to investigate the physics and chemistry of the ISM in these extreme environments. But many open questions still remain, such as: how the location of active formation of young massive stars correlates with that of the various molecular line tracers, or, what the ratios between molecular lines indicate about temperature, excitation and density structure in the gas.

NGC 6946 is an ideal candidate to study the effect of large and small scale bars on the dense gas and chemistry through molecular line emission. NGC 6946 has beside its large-scale stellar bar with a length of 100–120′ (≈ 3.7–4.5 kpc) (Regan & Vogel 1995; Menéndez-Delmestre et al. 2007; Font et al. 2014), a small-scale bar (see below), and is one of the nearest large double-barred spiral galaxies (D ≈ 7.72 Mpc; see Table 1). It does not seem to host an AGN (see Section 6.3) and leads the list of observed supernovae in a nearby galaxy disc (10 supernovae), which has led to its name Fireworks Galaxy.

In this work, we study the inner 50′ ≈ 1.9 kpc of NGC 6946, which has previously been the target for many multi-wavelength observations which we can use to compare to, and build upon,

---

2 [http://cbat.cfa.harvard.edu/lists/Supernovae.html](http://cbat.cfa.harvard.edu/lists/Supernovae.html)

---

for our analysis. We use ancillary 33 GHz continuum data (Murphy et al. 2018; Linden et al. 2020) to obtain the SFR from the free-free emission part to compare dense gas, total molecular gas, and extinction-free estimates of recent star formation across the inner star-forming centre of NGC 6946. In the sketch in Figure 1, we see in green colours three distinct regions in 12CO (2-1) (hereafter CO(2-1)). The appearance of these three features as an S-shaped structure have been explained with modelling efforts in Schinnerer et al. (2006). To do so, they obtained a three-dimensional representation of the luminosity and mass distribution of the galaxy using the multi-Gaussian expansion (MGE) method (see e.g. Emsellem et al. 2003). They then inferred the corresponding axisymmetric gravitational potential by using the Poisson equation and assuming a constant mass-to-light ratio, which is then perturbed by adding a ~ kpc bar-like structure to the MGE potential (as in Emsellem et al. 2003). They showed that their model reproduces the observed (straight) ~ kpc gas lane morphologies, when applying an inner bar with a radius of ≈ 250 pc (or 6.5–8′′ projected into the galaxy plane) with a pattern speed Ωp of 510–680 km s⁻¹ kpc⁻¹. They concluded that molecular gas flows inwards from the outer disc, shaping and driving the evolution of the centre of NGC 6946. Therefore, we refer to their ‘clumps’ as the bar ends of the inner bar (see green ellipses in the sketch of Figure 1). This allows us to study different regions in the centre: a) the nuclear region – NUC, b) the northern inner bar end – NBE, and c) the southern inner bar end – SBE, which we refer to as abbreviated above throughout this work.

In this work we present a suite of lines observed across the 1–3 mm IRAM Plateau de Bure Interferometer (PdBI) window [PI: E. Schinnerer] to assess the physical and chemical structure of the inner ~50′ of NGC 6946 (see Figures 2). This gives us one of the most comprehensive, high resolution (2–4′′ ≈ 75–150 pc) molecular line data set for a nearby galaxy centre in the northern hemisphere. In this first of a series of papers, we present the observations and especially focus on the short-spacing corrected bulk (CO) and dense gas tracers (HCN, HCO⁺ and HNC).

This paper is structured as follows: In Section 2, we present how the PdBI observations were taken, calibrated and imaged, along with information of the ancillary observations used within this work and how we convert observational measurements to physical quantities. Section 3 shows the results and Section 4 the discussion of our extended data set. In Section 5, we show the results from our short-spacing corrected data set focusing on the nuclear region and inner bar ends. In Section 6, we discuss line ratio diagnostics of the short-spacing corrected data set and possible implications for spectroscopic studies of other galaxy centres.

2. Observations and ancillary data

2.1. PdBI observations and data reduction

The Plateau de Bure Interferometer (PdBI) was used to image molecular lines at 1.3 to 3 mm using a single pointing focusing on the central 50′ of NGC 6946 for a total of 132 h from 2002 to 2009. Eight high-resolution spectral windows were used in each observation, each offering a bandwidth of 160 MHz and channel width of 2.5 MHz (i.e. 9 km s⁻¹ at 87 GHz). The data, acquired from multiple observations (project codes: Q059, R02C, R09F, S02A, R09F, S08E, P069, M032 and S02A; PI: Schinnerer), were split between five spectral setups at reference frequencies of ~87 GHz (setup A), ~97 GHz (setup B), ~92 GHz (setup C), ~115 GHz
Fig. 1. Gallery of the multi-wavelength observation towards the centre of NGC 6946. Left panels: (a) three colour optical image, with the region of interest drawn as a purple box, (b) CO (1-0) emission shown in contours levels of 60, 90, 200, 300, 600 K km\(^{-1}\) s\(^{-1}\), and are repeated on all panels for comparison, (c) integrated CO (1-0) emission, (d) CO (2-1) emission towards the inner 20\(''\) shown as colour scale; Sketch (right): denoting all observed features (see Section 2.4 for an overview), (e)–(g) continuum emission, (h)–(j) infrared emission and (k)–(m) hydrogen recombination lines and X-ray emission (see Table A.1 for references of all observations shown). The rightmost column shows integrated intensity maps of three of our fourteen detected emission lines for comparison. Optical image credits: NASA, ESA, STScI, R. Gendler, and the Subaru Telescope (NAOJ).
Table 1. Properties of NGC 6946

| Parameter          | Value          | Notes               |
|--------------------|----------------|---------------------|
| Morphology         | SAB(rs)cd      | (1)                 |
| Nuclear type       | star-forming, H II | (2)    |
| Age of starburst   | 7–20 Myr       | (3)                 |
| Distance.          | 7.72 Mpc       | (4)                 |
| Linear scale       | 37 pc/arcsec   |                     |
| Inclination        | 33°            | (5)                 |
| P.A. major axis    | 242°           | (6)                 |
| P.A. minor axis    | 152°           | (6)                 |
| \(v_{LSR}\)        | 50 km s\(^{-1}\) | (7)                 |

**Dynamic centre**

| R.A. (J2000) | 20:34:52.35 |
|-------------|-------------|
| Decl. (J2000) | +60:09:14.58 |
| Inner bar length | 6.5–8"     | (7)     |
| NBE, R.A.    | 20:34:51.71 | this work |
| NBE, Decl.   | +60:09:17.21 | this work |
| SBE, R.A.    | 20:34:52.67 | this work |
| SBE, Decl.   | +60:09:11.53 | this work |

Notes: (1): de Vaucouleurs et al. (1991); (2): Goulding & Alexander (2009); (3): Engelbracht et al. (1996); (4): Anand et al. (2018); they applied the tip of the red giant branch method to measure the distance to NGC 6946. The brightest red giant stars in the outer regions of NGC 6946 were adopted as standard candles. Research on NGC 6946 carried out before 2018 used smaller values for its distance, ranging from 5 Mpc (e.g. Schinnerer et al. 2006) to about 7 Mpc (e.g. Murpby et al. 2011). Where necessary, we convert measurements from the literature to our adopted distance. (5): de Blok et al. (2008); (6): Crosswhait (2002); (7): Schinnerer et al. (2006); (setup D) and ~230 GHz (setup one mm). We identified in the spectral setup A: \(\text{C}_2\text{H} (1-0), \text{HCO}^+ (1-0)\) and \(\text{HCN} (1-0)\), in setup B: \(\text{CH}_3\text{OH} (2-1), \text{CS} (2-1), \text{CH}_3\text{OH} (3-2), \text{HC}_3\text{N} (16-15), \text{H}_2\text{CO} (2-1)\) and CS (3-2), in setup C: \(\text{HNC} (1-0), \text{HC}_3\text{N} (10-9)\) and \(\text{N}_2\text{H}^+ (1-0)\), in setup D: \(\text{CO} (1-0)\), in setup one mm: \(\text{CO} (2-1)\) (see 2.2). The primary beam FWHM ranges from ~57\" at 87 GHz to ~43\" at 115 GHz and ~22\" at 230 GHz. The spectral window of each molecular line was centred on the redshifted frequency of the line assuming a systemic velocity of 50 km s\(^{-1}\) for NGC 6946 (Schinnerer et al. 2006). The imaged width in each spectral window is the velocity width at zero level of the CO (1-0) line (300 km s\(^{-1}\), matching the Full Width at Zero Intensity of the HI line seen by THINGS in Walter et al. (2008) plus 50 km s\(^{-1}\) on each side of the line centre. These data were all calibrated and imaged using GILDAS. For the bandpass calibration, observations of the bright quasars 3C454.3, 2145+067, 0923+392 and 3C273 have been used. The phase and amplitude calibrators were either both 2037+511 and 1928+738 or one of them. These calibrators were observed every 20 minutes. Most of the observations compared MWC 349 observations with its IRAM flux model to calibrate the absolute flux scale. We expect an accuracy of the flux calibration of about 5% at 3 mm and a typical antenna aperture efficiencies of about 25 Jy K\(^{-1}\) at 3 mm, and 28 Jy K\(^{-1}\) at 2 mm data.

The continuum emission has been combined with the UV MERE task after excluding the line channels. The spectral lines were resampled to 10 km s\(^{-1}\) for all the lines during the creation of UV tables in the GILDAS CLIC environment. The continuum has been subtracted in the \(u-v\) plane with the above continuum \(u-v\) table extracted from all line-free channels with the UV SUBTRACT task before the imaging. Imaging of the visibilities used natural weighting, where each visibility is weighted by the inverse of the noise variance, as this maximises the sensitivity. The field of view of each image is twice the primary beam with pixel sizes 1/4 of the synthesised beam major axis FWHM size (ranging from 0.4" × 0.29" to 2.0" × 1.7" and 3.6" × 2.9" see Table 3).

Cleaning was performed with a preconstructed clean mask which has been produced similar to the signal identification methodology used in CPRoPS (Rosolowsky & Leroy 2006; Rosolowsky et al. 2021; Leroy et al. 2021) using the high resolution (~1") CO (1-0) PdBI data without short-spacing correction (Schinnerer et al. 2006). Following Leroy et al. (Leroy et al. 2021; for the PHANGS-ALMA survey), the clean mask creation includes the following steps: (a) convolving the CO (1-0) beam from ~1" to a coarser resolution of 33" and smoothing along the spectral axis with a boxcar function with a width of 20 km s\(^{-1}\), (b) selecting peak pixels for each channel which have a S/N of at least 4; (c) expanding each peak down to a S/N of 2; (d) binarilating 4 channels along the spectral axis to account for edge effect. This produces a clean mask that covers all possible CO signal regions and ensures that the cleaning of other molecular gas tracers is less affected by noisy, no-signal regions outside the mask. The typical rms per channel observed is \(\approx 2\) mJy beam\(^{-1}\).

Before being used in the deconvolution, the clean mask was regrided to match the astrometry of the dirty cube of each line. After imaging and deconvolution we corrected for the primary beam attenuation. We provide the observational characteristics of the PdBI only data in Table 3 (and show the channel maps in Fig. A.3–A.14).

Given that these data have different \(u-v\) coverage, we built a homogenised product by imaging only the visibilities that are within the \(u-v\) coverage of the CO (1-0) PdBI data, that is 11.5 to 153.8 kλ. We do this to match the spatial scales of the CO data. This has been done using a GILDAS script where we loop through all the visibilities and flag the ones outside the CO (1-0) \(u-v\)-range by assigning negative weights to them. Then the UV TRIM function was used to discard the flagged data.

Interferometric observations are insensitive to emission with low spatial frequencies due to the lack of the shortest baselines. For the short-spacing correction, we utilise IRAM 30 m observations. We use data of the EMIR Multiline Probe of the ISM Regulating Galaxy Evolution (EMIPE; Jiménez-Donaire et al. 2019) survey which observed in the 3–4 mm regime, in particular, HCN across the whole disc of nine nearby spiral galaxies, among them NGC 6946. For the purpose of the short-spacing correction (SSC) we use their 33" resolution HCN (1-0), HCO\(^+\) (1-0) and HNC (1-0) maps. For the CO (2-1) observations, we use data from the HERA CO-Line Extragalactic Survey (HERACLES) (Leroy et al. 2009). For the remaining PdBI detected molecules we do not find public single-dish data with a significant S/N\(^2\), therefore, no SSC was feasible for them.

SSC has been done in GILDAS in its MAPPING environment. Before performing SSC on the data available, we ensured that the 30 m data used the same projection center and spectral grid as the interferometric data, before applying the UVSHIFT task. This produces pseudo-visualisibilities that fill the short-spacings before imaging and deconvolution (see Rodríguez-Fernandez et al. 2006). We note that the 3mm emission lines of \(\text{C}_2\text{H}, \text{N}_2\text{H}^+\), and \(\text{HC}_3\text{N}\) were covered by EMIPE, but not included in the public release.

\(^3\) http://www.iram.fr/IRAMFR/GILDAS
Table 2. Summary of the molecular lines in our compiled data set towards the centre of NGC 6946.

| Molecules | $T_{\text{rest}}$ (K) | $v_{\text{obs}}$ (GHz) | $E_a$ (K) | $n_{\text{eq}}$ ($\epsilon_{\text{max}}$) (cm$^{-3}$) | $n_{\text{off}}$ (cm$^{-3}$) | project code | setup |
|-----------|----------------|------------------|--------|----------------|----------------|----------|-------|
| CH$_3$OH  | (1–0) | 90.664 | 90.648 | 4.35 | $1 \times 10^3$ | $2.3 \times 10^3$ | Q059+R02C | C     |
| HCN      | (10–9) | 90.979 | 90.964 | 16.69 | $4.3 \times 10^4$ | R09F | C     |
| HCO$^+$  | (1–0) | 93.174 | 93.158 | 4.47 | $5.5 \times 10^4$ | R09F | C     |
| CH$_3$OH | $J_k = 2n-1_0$ | 96.741 | 96.725 | 6.96 | $2.7 \times 10^5$ | Q059+R02C | B     |
| CS       | (2–1) | 97.980 | 97.965 | 7.10 | $1.2 \times 10^4$ | R09F+S08E | B     |
| $^{12}$CO | (1–0) | 115.271 | 115.252 | 5.53 | $1 \times 10^5$ | M032 | D     |
| CH$_3$OH | $J_k = 3n-2_0$ | 145.100 | 145.073 | 18.80 | $2.5 \times 10^5$ | S02A | B     |
| HCN$^*$  | (16–15) | 145.561 | 145.534 | 41.27 | $2.5 \times 10^5$ | S02A | B     |
| p-H$_2$CO | $N = (2-1), J = 0/2-0/1$ | 145.603 | 145.576 | 10.48 | $6.3 \times 10^5$ | S02A | B     |
| CS       | (3–2) | 146.969 | 146.942 | 14.11 | $3.3 \times 10^5$ | S02A | B     |
| $^{13}$CO | (2–1) | 230.338 | 230.499 | 16.59 | $1 \times 10^5$ | M032+P069 | one mm |

Notes: (1–2): Molecular lines with their transition ordered by their rest frequencies; Throughout the paper, for simplicity, we refer to the transitions of CH$_3$OH as (1–0), of CH$_3$OH as (2–1) and (3–2), and of H$_2$CO as (2–1); (3–4): Rest and observational frequencies; (5): Upper energy levels; (6): Minimum density at which the emissivity of the line reaches 95% of its peak value for $T = 25$ K (see table 2 within Leroy et al. 2017 and references therein); (7): Taken from Shirley (2015) (table 1, for K), and have been defined by radiative transfer modelling as that density at which the luminosity of the line is that in a molecular line with an integrated intensity of 1 K km s$^{-1}$; (8–9): PdBI project code and setup. A = configuration C and D; B = configuration A, B, C, D; C = configuration B, C, D.

| Molecules (1) | Native resolution | Beam size (" (2) | P.A. (3) | $I_{\text{line}}$ [K km s$^{-1}$ (4)] | $T_{\text{peak}}$ [K] (5) | Characteristics at 4$''$ resolution | Ratios with CO (6) | CO (2–1) (8) | CO (1–0) (9) | HCN (10) | $\Sigma_{\text{SFR}}$ (11) |
|---------------|-------------------|-----------------|--------|-------------------|-------------------|-----------------|----------------|----------------|----------------|----------|----------------|
| $^{12}$CO (1–0) | 1.36 x 1.11 | 26 | 748.04 | 8.80 | 2.85 | 262.72 | 1.00 | 13.04 | 8.31E+01 |
| $^{13}$CO (2–1) | 0.40 x 0.29 | 91 | 296.40 | 4.75 | 2.20 | 134.56 | 1.00 | 5.17 | 3.29E+01 |
| HCN (1–0) | 2.61 x 2.12 | 97 | 57.35 | 0.62 | 0.71 | 80.65 | 0.19 | 1.00 | 6.37E+00 |
| HCO$^+$ (1–0) | 3.45 x 2.83 | -101 | 47.94 | 0.53 | 0.52 | 92.43 | 0.16 | 0.84 | 5.31E+00 |
| HNC (1–0) | 2.45 x 2.00 | 62 | 22.06 | 0.32 | 0.62 | 35.66 | 0.07 | 0.38 | 2.45E+00 |
| CS (2–1) | 1.89 x 1.60 | 97 | 29.39 | 0.40 | 0.72 | 40.57 | 0.01 | 0.51 | 3.26E+00 |
| CS (3–2) | 1.98 x 1.76 | -180 | 21.07 | 0.30 | 0.28 | 76.00 | 0.07 | 0.37 | 3.24E+00 |
| N$_2$H$^+$ (1–0) | 2.39 x 1.96 | 65 | 6.43 | 0.21 | 0.49 | 13.02 | 0.02 | 0.11 | 7.14E-01 |
| HCN (10–9) | 2.41 x 1.98 | 64 | 4.06 | 0.09 | 0.68 | 5.93 | 0.01 | 0.07 | 4.51E-01 |
| HCN (16–15) | 2.02 x 1.77 | 339 | 2.25 | 0.08 | 0.39 | 5.72 | 0.01 | 0.04 | 2.50E-01 |
| CH$_3$OH (2k-1k) | 1.89 x 1.59 | 98 | 7.15 | 0.27 | 0.66 | 10.77 | 0.02 | 0.12 | 7.95E-01 |
| CH$_3$OH (3k-2k) | 1.98 x 1.76 | -17 | 6.12 | 0.28 | 0.55 | 11.09 | 0.02 | 0.11 | 6.80E-01 |
| C$_2$H (1-0)/3-2/1-2 | 3.54 x 2.84 | 77 | 12.78 | 0.14 | 0.72 | 17.76 | 0.04 | 0.22 | 1.42E+00 |
| H$_2$CO (2–1) | 1.99 x 1.75 | 343 | 2.29 | 0.08 | 0.35 | 6.61 | 0.01 | 0.04 | 2.54E-01 |

Notes: We arranged the $PdB1$ only data set as in Fig. 3 and show them at their native and best-common 4$''$ $\approx$ 150 pc spatial resolution. Column (1): Molecules and their transitions. (2–3): Characteristics of the native resolution observation. (4–11): We quote the mean for the central sight line, i.e. aperture of 4$''$ $\approx$ 150 pc: (4): Integrated intensity. (5): Peak temperature of the spectrum. (6): Root mean square (rms) noise. (7): Signal to noise. (8–11): Ratios of molecular species with CO, HCN and $\Sigma_{\text{SFR}}$. The $I_{\text{line}}/\Sigma_{\text{SFR}}$ ratio results in units of K km s$^{-1}$/(M$_{\odot}$ yr$^{-1}$ kpc$^{-2}$).

2008; Pety et al. 2013 for details). We summarise the observational characteristics of the SSC + $u-\nu$ trim data in Table 4.

In summary, within this work we make use of the following data sets: $PdB1$ only, which includes 14 molecular emission lines, and SSC + $u-\nu$ trim, which includes five molecular emission lines.

2.2. Integrated intensity maps

As a next step, we converted our $PdB1$ only and SSC + $u-\nu$ trim data cubes from units of Jy beam$^{-1}$ to brightness temperature, $T_B$, measured in Kelvin. Our observations include emission lines from a wavelength range of 1 to 3 mm which results in various spatial resolutions. We convolved our data to a common beam size of 4$''$ (corresponding to 150 pc at 7.72 Mpc distance) and sampled the integrated intensities onto a hexagonal grid. The grid points are spaced by half a beam size to approximately Nyquist sample the maps. This approach has the advantage that the emission lines can be directly compared.

To improve the signal-to-noise ratio (S/N) we applied a masking routine for the determination of the integrated intensity maps. We used the bright CO (1–0) emission line as a prior for
masking and produced two S/N cuts: a low S/N mask (S/N > 2) and a high S/N mask (S/N > 4). Subsequently, the high S/N mask is expanded into connected voxels in the low S/N mask, and the integrated intensity is determined by integrating along the velocity axis for each of the individual sight lines multiplied by the channel width, \( \Delta v_{\text{chan}} \), of 10 km s\(^{-1}\):

\[
I = \sum_{n_{\text{chan}}} T_{B} \times \Delta v_{\text{chan}}.
\]

(1)

The uncertainty is calculated taking the square root of the number of masked channels (\( n_{\text{chan}} \)) along a line of sight multiplied by the 1\( \sigma \) root mean square (\( \sigma_{\text{rms}} \)) value of the noise and the channel width:

\[
\sigma_{I} = \sqrt{n_{\text{chan}}} \times \sigma_{\text{rms}} \times \Delta v_{\text{chan}}.
\]

(2)

We calculate \( \sigma_{\text{rms}} \) over the signal-free part of the spectrum using the astropy (Astropy Collaboration et al. 2013, 2018) function mad_std that calculates the median absolute deviation and scales it by a factor of 1.4826. This factor results from the assumption that the noise follows a Gaussian distribution. We show the integrated intensity maps of the PdBI only data in Fig. 2.

### 2.3. Ancillary data

We include ancillary data for investigating the central regions of NGC 6946 and analysing the relationship of our detected molecules to star formation rate (SFR) tracers. We also compare NGC 6946 with other galaxy centers. Therefore, we include (1) 33 GHz continuum emission, (2) EMPIRE dense gas observations of eight additional galaxy centres (angular resolution of 3\( \arcsec \) ≈ 1 kpc), (3) high resolution resolution dense gas observations of M 51 (~4\( \arcsec \) ≈ 166 pc) and NGC 3627 (~2\( \arcsec \) ≈ 100 pc), and (4) 0.5–7.0 keV X-ray observations of NGC 6946.

### 2.3.1. SFR tracers

Tracers of the number of ionizing photons, specifically free-free emission of ionizing continuum and hydrogen recombination lines, are often regarded as good indicators of massive star formation. The radio continuum emission at low frequencies consists of two components: (1) thermal free-free emission directly related to the production rate of ionizing photons in H II regions and (2) non-thermal emission arising from cosmic ray electrons or positrons which propagate through the magnetised ISM after being accelerated by supernova remnants or from AGN. Concentrating on the first case, only stars more massive than ~8 \( M_{\odot} \) are able to produce a measurable ionising photon flux (see e.g. Murphy et al. 2012; Kennicutt & Evans 2012).

For NGC 6946 we find recently published 33 GHz continuum emission, which best matches with the angular resolution of our molecular data set (~2.1\( \arcsec \)) angular resolution, see Fig. 1g and Fig. 4). These data are from Very Large Array (VLA) observations within the Star Formation in Radio Survey (SFRS; Murphy et al. 2018; Linden et al. 2020). In this work, we use the (1) thermal free-free emission of the 33 GHz continuum emission as a SFR tracer (see below). We discuss the reasons why we preferred 33 GHz and check for consistency in the Appendix A.

#### 2.3.2. Calibration of the SFR

The calibration of a variety of SFR indicators has been described in detail by Murphy et al. (2011). They used Starburst99 (Leitherer et al. 1999) together with a Kroupa (2001) initial mass function (IMF). This type of IMF has a slope of −1.3 for stellar masses between 0.1 and 50 \( M_{\odot} \), and a slope of −2.3 for stellar masses ranging between 0.5 and 100 \( M_{\odot} \). Together with their assumptions of a continuous, constant SFR over ~100 Myr, their Starburst99 stellar population models show a relation between the SFR and the production rate of ionizing photons, \( Q(H^{0}) \), as:

\[
\text{SFR} = \frac{7.29 \times 10^{-34} Q(H^{0})}{[\text{s}^{-1}]}.
\]

(3)

For the 33 GHz continuum map, we need to separate the (1) thermal free-free and (2) non-thermal (synchrotron) parts of the emission. The thermal emission (denoted by \( T \)) scales as \( S_{T} \propto \nu^{-\alpha} \), where \( \nu \) refers to the frequency in GHz. To convert the thermal flux into a SFR, we follow Eq. (11) from Murphy et al. 2011:

\[
\text{SFR}_{T} = 4.6 \times 10^{-28} \left( \frac{T_{e}}{[10^{4} \text{K}]} \right)^{-0.45} \times \left( \frac{\nu}{[\text{GHz}]} \right)^{-3} \frac{L_{T}^{\frac{1}{2}}}{[\text{erg s}^{-1} \text{Hz}^{-1}]}.
\]

(4)

where \( T_{e} \) is the electron temperature in units of 10\(^4\) K, \( \nu \) refers to the frequency in GHz, and \( L_{T}^{\frac{1}{2}} \) is the luminosity of the free-free emission at frequency \( \nu \) in units of erg s\(^{-1}\) Hz\(^{-1}\).
We adopt $\alpha_T = 0.1$ and a thermal fraction of $f_{33\text{GHz}}^T = 0.62$ (as in Murphy et al. 2011 for the nucleus of NGC 6946) and calculate the luminosity of the thermal free-free emission at frequency $\nu$:

$$L_\nu^T = \frac{\nu^3 L}{(\nu - 33\text{GHz})^2},$$

(5)

Together with $T_e = 0.42$ in units of $10^4$ K (again as in Murphy et al. 2011 for the nucleus of NGC 6946) and Eq. (5) we can solve Eq. (4) and get a SFR$_{150\text{GHz}}$ map in units of $M_\odot$ yr$^{-1}$. We discuss the mean values within 150 pc sized apertures (i.e. the 4$''$ working resolution) containing the NUC, SBE, or NBE regions in Section 4. In this work, we also use SFR surface densities ($\Sigma_{\text{SFR}}$) in units of $M_\odot$ yr$^{-1}$ kpc$^{-2}$ for scaling relations in Section 5.2. We define $\Sigma_{\text{SFR}}$ as:

$$\Sigma_{\text{SFR}} = \frac{\text{SFR}_{33\text{GHz}}}{M_\odot \text{yr}^{-1}} \left(\frac{\Omega}{\text{kpc}^{-2}}\right)^{-1},$$

(6)

where $\Omega$ is:

$$\Omega = \pi \left(\frac{\theta_{\text{maj}}}{\text{arcsec}}\right) \left(\frac{d}{\text{kpc}}\right) \psi^{-1} \times \left(\frac{\theta_{\text{min}}}{\text{arcsec}}\right) \left(\frac{d}{\text{kpc}}\right) \psi^{-1} \times (4 \ln(2))^{-1}.$$  

(7)

Here, $\theta_{\text{maj}}$ and $\theta_{\text{min}}$ are the major and minor axis of the beam in arcsec, $d$ the distance to NGC 6946 in kpc and $\psi$ is the factor to convert from rad to arcsec (i.e. $3600 \times 180)/\pi$).

### 2.3.3. Molecular gas mass and depletion time

The molecular gas mass surface density can be estimated from the CO (1-0) line emission in our data set. Given that H$_2$ is the most abundant molecule, the conversion of CO emission to molecular gas mass surface density is related to the CO-to-H$_2$ conversion factor $\alpha_{\text{CO}}$. We adopt a fixed conversion factor $\alpha_{\text{CO}} = 0.39 M_\odot \text{pc}^{-2} (\text{K km s}^{-1})^{-1}$ corrected for helium (Sandstrom et al. 2013; from their Table 6 for the centre of NGC 6946). This low, central $\alpha_{\text{CO}}$ value of NGC 6946 (a factor $\sim 10$ lower than the canonical Milky Way value of $4.36 M_\odot \text{pc}^{-2} (\text{K km s}^{-1})^{-1}$; see Bolatto et al. 2013) agrees with other studies (e.g. Cormier et al. 2018; Bigiel et al. 2020) and will not affect the main results in this paper. Then we convert the CO (1-0) integrated intensity, $I_{150\text{pc}}^{\text{mol}}$, to the molecular gas mass surface density, $\Sigma_{\text{mol}}$, via:

$$\Sigma_{\text{mol}} = \alpha_{\text{CO}} I_{150\text{pc}}^{\text{mol}} \left(\frac{K \text{ km s}^{-1}}{\text{pc}}\right) \cos(i).$$

(8)

Here, $I_{150\text{pc}}^{\text{mol}}$ stands for $I_{150\text{pc}}^{\text{mol}}$ convolved to 150 pc (4$''$) FWHM and the $\cos(i)$ factor corrects for inclination. We note, that the conversion from observed to physical quantity is subject to uncertainties for example, the low-J transition of $^{12}\text{CO}$ is known to be optically thick and does not necessarily peak in the 1-0 transition in many environments. Together, this may result in a less accurate CO to H$_2$ conversion, particularly towards starburst or AGN regions, yet this is most likely still secondary compared to the uncertainty on the $\alpha_{\text{CO}}$ (e.g. due to metallicity). The ratio of the two profiles $\Sigma_{\text{mol}}/\Sigma_{\text{SFR}}$ is the molecular gas depletion time, the time it takes (present day) star formation to deplete the current supply of molecular gas:

$$\tau_{\text{depl,150pc}} = \frac{\Sigma_{\text{mol}}}{\text{M}_\odot \text{pc}^{-2}} \frac{\Sigma_{\text{SFR}}}{\text{M}_\odot \text{yr}^{-1} \text{kpc}^{-2}} \left(\frac{\gamma}{\text{[kpc}^2/\text{pc}^2]}\right)^{-1}. $$

(9)

Here, $\gamma$ stands for the conversion factor to get from kpc$^{-2}$ to pc$^{-2}$. Eq. 9 implies that all the molecular gas traced by CO will turn into star formation fuel which is an overestimate. We use CO to define $\tau_{\text{depl,150pc}}$ because we later compare it to literature values that used the same method to calculate $\tau_{\text{mol}}$; this does not affect the main results of this work.

### 2.3.4. EMPIRE dense gas data, high-resolution M 51 and NGC 3627 data

In Section 6 we discuss line ratio diagnostic plots of the dense gas tracers HCN, HCO$^+$ and HNC. To compare NGC 6946 with other galaxy centres, we use available observations of additional eight galaxy centres (see legend in Fig. 8d) covered in the EMPIRE survey (Jiménez-Donaire et al. 2019). Those data products have a common angular resolution of 33$''$ ($\approx 1$ kpc). For the analysis in Section 6.3 we also include high resolution observations of the dense gas tracers for: (i) M 51 and (ii) NGC 3627. The M 51 short-spacing corrected observations have an angular resolution of $\sim 4''$ ($\approx 166$ pc) and their reduction are described in Querejeta et al. 2016. We used the same technique as for the NGC 6946 observations described in Section 2.2 to sample the data on a hexagonal grid and produce integrated intensity maps with a common angular resolution of 4$''$. We have also done this for the NGC 3627 observations, which have an angular resolution of $\sim 2''$ ($\approx 100$ pc); their short-spacing correction and reduction are described in Bešlić et al. 2021.

### 2.3.5. X-ray

We also compare our observations to Chandra ACIS-S observations (ObsIDs 1054 and 13435) from 2001 (PI: S. Holt; Holt et al. 2003) and 2012 (PI: C. Kochanek) totalling 79 ks. We reduced the data using the Chandra Interactive Analysis of Observations (ciao) Version 4.9 and produced exposure-corrected images using the ciao command mergeObs. Point sources were identified using wavdetect on the merged, broadband (0.5–7.0 keV) image and were removed with dmfilth to create the X-ray image shown in Fig. 8. We also show a version of the X-ray diffuse, hot gas that has been smoothed with a Gaussian kernel (FWHM of 3) in Fig. 1 (m).

### 2.4. Multi-wavelength gallery of the central region of NGC 6946

Fig. 1 shows a compilation of the various observations towards the inner 50$''$ $\approx 1.86$ kpc of NGC 6946 (see Table A.1 for details on the observations). The centre appears to have several branches that connect to the outside environment. The two more pronounced spiral-like structures running north and south (extending 50$''$) are most apparent in $^{12}\text{CO}(1-0)$ (published in Schinnerer et al. 2006) (c) and to some extent also in the infrared emission (h–(j)). Another spiral-like structure could be presumed from these observations. Preceding studies even assumed four spiral features (Regan & Vogel 1995), which are not apparent in this CO map. The sketch on the top right shows...
the two prominent spiral-like structures and the third presumable one as blue coloured arcs.

The red coloured ellipse in the sketch (extending 20′′ ≈ 750 pc) denotes the radio continuum emission (e)–(g). In the 70 μm, 24 μm, 8 μm, Paβ, Hα and X-ray emission (h)–(m), we likewise find emission in this region. In maps (e)–(m), however, no substructures are visible within the red ellipse due to high saturation or limited angular resolution. In contrast to that, CO (2–1) reveals the nuclear region and two additional features to the north and south, illustrated as green ellipses in the sketch (central ~10″ ≈ 372 pc). Schinnerer et al. (2006) showed with dynamical models that the structures of CO (2–1) can be explained with an inner bar (first observed and proposed via FIR by Elmegreen et al. 1998). The two inner bar ends (NBE and SBE) are connected to the nuclear region by straight gas lanes running along a position angle of P.A. ~40°. Those regions are also bright in emission in HCN, HCO+ and HNC (see Section 3).

The four additional red ellipses in the sketch, most visible in the continuum emission (e)–(f), were identified by Linden et al. (2020). The southern two are associated with star formation (SF) regions and the northern two are suggested to be anomalous microwave emission (AME) candidates (Linden et al. 2020). The exact mechanism causing AMEs is not entirely understood, but the most promising explanation is that they occur due to small rotating dust grains in the ISM (see the review on AMEs by Dickinson et al. 2018). One of the techniques to identify AMEs is to investigate the 33 GHz/Hα flux ratio (Murphy et al. 2018).

Larger ratios of 33 GHz flux to Hα line flux would arise by an excess of non-thermal radio emission (see Fig. 4 in Murphy et al. 2018; ratios of ~10^3). Using 7″ apertures in diameter for the two AME candidates we find 33 GHz/Hα ratios of ~10^3 expected for AME emission. This would confirm them being AME candidates.

Within the southern SF region, at the end of the CO (1–0) southern spiral structure, Gorski et al. (2018) found a water maser (H2O (6_16–5_23) at 22.235 GHz) and within the southern inner bar end two methanol masers (CH3OH (4_1–3_0) at 36.169 GHz), marked as blue and orange stars in the sketch. The water maser is associated with one of the identified SF regions of Linden et al. (2020). Water masers can be in general variable on timescales of a few weeks and could indicate YSOs or AGB stars (Palagi et al. 1993). Billington et al. (2020) showed within the Milky Way the relationship between dense gas clumps and water masers. The location of the water maser matches well with the SF region seen in the Hα and 33 GHz maps.

### 3. Results – Molecules in different environmental regions in the centre of NGC 6946

We investigate how the molecular species in our data set spatially vary in the inner kiloparsec of NGC 6946. Our compiled data set contains 14 molecular emission lines obtained with the IRAM PdBI covering the inner 50″ ≈ 1.9 kpc of NGC 6946, which are summarised in Table 3. Their intensity maps can be seen in Fig. 2 showing the integrated intensities for the detected molecular lines.

#### 3.1. The substructures in the inner kiloparsec of NGC 6946

In every map of Fig. 2 we detect significant emission in the inner 10″ ≈ 375 pc. We note that we have for the first time detected ethynyl C2H (1–0), cyanoacetylene HCN (10–9) and HC3N (16–15) in the inner kiloparsec of NGC 6946. All other molecules have been detected previously, mostly at lower resolution (e.g. ~30″ HNC (1–0) and N2H+ (1–0); Jiménez-Donaire et al. 2019; 25″ and 17″ CH3OH (2–1), CH3OH (3–2), H2CO (2–1): Kelly et al. 2015; 8″ HCO+ (1–0): Levine et al. 2008; 1″ HCN (1–0): Schinnerer et al. 2007).

#### The spiral structures: We see several branches that seem to be connected to the outside environment. The two more prominent spiral-like structures are best visible in the integrated intensity map of CO (1–0) tracing the bulk molecular gas. For comparison with the other molecular species, we plot red contours of CO (1–0) with S/N levels of 30,60,90 showing the spiral directions in the north and south in all of the 14 maps. The white S/N contours of HCN (1–0), HCO+ (1–0) and HNC (1–0) overlap with the northern spiral structure (labelled as ‘s1’ in the sketch in Fig. 1). The southern spiral (s2) is visible in HCN (1–0), HCO+ (1–0), HNC (1–0) and N2H+ (1–0). We denoted a third spiral (s3), which is present in HCN (1–0), HCO+ (1–0), HNC (1–0), N2H+ (1–0), CS (2–1) and CH3OH (2–1).

The inner bar and nuclear region: Already inferred in the sketch in Fig. 1 from the native resolution CO (2–1) data, we know the location of the inner bar ends (NBE and SBE) and the nuclear region (NUC), and are able to investigate them with our other molecular emission lines. Considering only the integrated intensities with S/N > 5 in each of the maps in Fig. 2, we see that the small-scale distributions of molecular species vary in these environments and that they do not necessarily peak at the same locations (see Table 5).

While in the strongest lines, CO (1–0), CO (2–1), HCN (1–0), HCO+ (1–0) and HNC (1–0), all these regions are evident and their integrated intensities are peaking in the NUC, the situation becomes different for molecular species with higher effective critical densities. In particular, CS (3–2) and C2H (1–0) show emission concentrated to the inner 5″ radius. Contrary to that, the highest integrated intensities are not peaking at the

---

**Table 5. Spatial distribution comparison of the molecular species.**

| Species     | s1 | s2 | s3 | NBE | SBE | NUC |
|-------------|----|----|----|-----|-----|-----|
| 12CO (1–0)  | ✓  | ✓  | ✓  | ✓   | ✓   | ✓   |
| 13CO (2–1)  | ✓  | ✓  | ✓  | ✓   | ✓   | ✓   |
| HCN (1–0)   | ✓  | ✓  | ✓  | ✓   | ✓   | ✓   |
| HCO+ (1–0)  | ✓  | ✓  | ✓  | ✓   | ✓   | ✓   |
| HNC (1–0)   | ✓  | ✓  | ✓  | ✓   | ✓   | ✓   |
| CS (2–1)    | ✓  | ✓  | ✓  | ✓   | ✓   | ✓   |
| CS (3–2)    | ✓  | ✓  | ✓  | ✓   | ✓   | ✓   |
| N2H+ (1–0)  | ✓  | ✓  | ✓  | ✓   | ✓   | ✓   |
| HC3N (16–15)| ✓  | ✓  | ✓  | ✓   | ✓   | ✓   |
| H2CO (2–1)  | ✓  | ✓  | ✓  | ✓   | ✓   | ✓   |

Notes: The comparison is based on their S/N > 5 peaks in the integrated intensity maps (see Figure A.2 in the Appendix). We consider the three spiral structures (s1–s3), the inner bar ends (NBE and SBE) and the nuclear region (NUC). ✓ denotes that we find within this region a S/N > 5 detection, ✓ not; ✓✓ refers to the location of the peak maximum in integrated intensity in the inner 50″ ≈ 1.9 kpc.
very centre for HC$_3$N (10-9), N$_2$H$^+$ (1-0), CH$_3$OH (2-1) and CH$_3$OH (3-2). Their peaks in emission are in the southern inner bar end. Interestingly, in the CS maps we do not see a peak in the SBE, although their $n_{\text{eff}}$ is higher than N$_2$H$^+$ which peaks in the SBE. Of course, the different distributions of the molecular emissions may not be a direct result of the density difference,
but also temperature (e.g. driven by the embedded star formation) that could drive both excitation and abundance variations. Table 5 compares the spatial distribution of various molecular species.

3.2. Molecular line profiles towards the nuclear region and what they are indicating

Fig. 3 shows the spectra of all the detected molecules for the central sight line (4′′ ≈ 150 pc aperture). For visualisation purposes we normalised them to the maximum value in their spectra. We investigate what the molecular species in our data set reveal about the physical state of the molecular gas at the centre of NGC 6946.

CO is tracing the bulk molecular gas content and its line brightness is up to a factor of 14 higher than other molecular lines within this work (see Table 3). Relative to CO, molecules such as HCN are tracing denser gas, as they get excited at effective densities of $n \geq 10^5$ cm$^{-3}$. As we go up in $n_{\text{eff}}$, HNC, N$_2$H$^+$, CS and HC$_3$N are potentially tracing even denser molecular gas. This means, HC$_3$N is tracing the densest molecular gas in our data set. The spectrum in Fig. 3, however, shows that HC$_3$N has in the central 150 pc the lowest S/N among all our molecular emission lines (S/N of 6). However, as we could see in Table 5, their maximum integrated intensities are located in the SBE, and there we find a S/N of 11 and 36.

Among our molecular species, there are some that reveal more about the chemistry of the gas. The formation path of ethynyl (C$_2$H) is favoured in PDRs by the reaction of C$^+$ with small hydrocarbons and additionally through photodissociation of C$_3$H$_2$ (Meier & Turner 2005, and references therein). This means enhanced C$_2$H in PDRs associated with massive hot cores indicates hidden star formation (Martín et al. 2015; Harada et al. 2018). Recently, Holdship et al. (2021) showed in the nucleus of NGC 253 that high abundances of C$_2$H can be caused by a high cosmic ray ionization rate. We detect C$_2$H (1−0) towards the nuclear region of NGC 6946 and the line shows similar to CO and dense gas tracers a broad line profile (FWHM≈200 km s$^{-1}$) including two peaks.

Strong methanol (CH$_3$OH) emission is considered a tracer of shocks (e.g. Saito et al. 2017). The reason for this is the formation process of CH$_3$OH in the gas phase is not efficient enough to produce higher amounts of CH$_3$OH (Lee et al. 1996). Intense CH$_3$OH emission is believed to arise from a series of hydrogenations of CO on dust grain surfaces under a low-temperature condition (Watanabe et al. 2003). After production on dust, it needs energetic heating mechanisms – shock chemistry – (e.g. Viti et al. 2011; James et al. 2020) to heat the dust and then sublimate CH$_3$OH into the gas phase. However, methanol emission can also be enhanced in non-shocked environments, such as towards massive stars or sources of cosmic ray or X-rays that heat the dust to ~100 K and allow methanol to evaporate into the gas phase. In our data set, both methanol transitions are stronger in their line brightness than the faintest dense gas tracers – N$_2$H$^+$ and HC$_3$N. Also, both methanol tracers have their maximum integrated intensity peaks in the SBE, where their ratios with CO are higher ($I_{\text{CH}_3\text{OH}}/I_{\text{CO}(2-1)}$). Methanol is also known to be a good kinetic temperature probe (e.g. Beuther et al. 2005). Furthermore, para-H$_2$CO transitions can also be used as a temperature indicator which is sensitive to warmer ($T > 20$ K) and denser ($n \sim 10^4$–$10^5$ cm$^{-3}$) gas (e.g. Ginsburg et al. 2016; Mangum et al. 2019). H$_2$CO can be formed in the gas phase as well as on the surface of dust grains (e.g. Terwisscha van Scheltinga et al. 2018).
respectively. We note, however, that each molecule is not a unique tracer of a particular process or sets physical conditions in a galaxy. To highlight this point, C$_2$H (1–0), for example, in the Milky Way is a tracer of PDRs, yet in NGC 1068 or NGC 253 it is tracing a completely different type of gas (García-Burillo et al. 2017; Holdship et al. 2021). In NGC 1068 it appears to trace a turbulent extended interface between outflows and ISM, yet in NGC 253 it appears to trace the dense gas that is subject to enhanced cosmic-ray ionization rates. Modelling can shed some light on the interpretation, and will be the subject of future work.

Schinnerer et al. (2006) found that the profiles of CO (1–0) and CO (2–1) are double peaked in NGC 6946. In Fig. 3 we also notice double-peaked profiles in the spectra of HCN (1–0), HCO$^+$ (1–0), HNC (1–0), CS (2–1), CS (3–2), HCN (10–9), N$_2$H$^+$ (1–0), C$_2$H (1–0), CH$_3$OH (2–1) and CH$_3$OH (3–2). These could be due to differential Galactic velocities and/or outflows in the central 4″$\approx$150 pc. A more detailed analysis of the kinematics and dynamics of these spectral features are not discussed in this paper but is planned for a future publication.

In Fig. 3 we denote the peak S/N and what condition each of the molecules can potentially indicate on the right-hand side.

4. The environmental variability of the star formation rate in NGC 6946

We seek answers to how the molecular lines in our data set relate to the current star formation rate (SFR) and if the different environments vary in their SFR on 150 pc scales, or if they have similar characteristics in this respect. We show a map of SFR in panel (a) of Fig. 4 with contours of tracers of denser gas HCN (1–0) and HNC (1–0), and shock tracer CH$_3$OH (3–2) at their native resolution (see Table 2). SFR is peaking at the very centre and drops towards the NBE and SBE. To further investigate these differences and the correlations between SFR and the molecular lines in our data set, we convolve the SFR map with units of M$_\odot$ yr$^{-1}$ to our working resolution of 4″$\approx$150 pc and sampled it onto a hexagonal grid to match with our integrated intensity maps. The white contours in panel (b) of Fig. 4 show the CO (2–1) emission indicating the three distinct features – the nuclear region (NUC) and the northern and southern inner bar ends (NBE and SBE). Since integrated intensities of our dense gas tracers are higher in the SBE than in NBE, we expect to find higher SFR in SBE.

In the following we quote SFR values for the NUC, SBE and NBE which have been averaged over these 150 pc sized regions. As expected, we find the highest SFR within the NUC, 0.089 M$_\odot$ yr$^{-1}$. But we see differences in the other two regimes: higher SFR in the SBE than in NBE, 0.013 and 0.006 M$_\odot$ yr$^{-1}$, respectively. This agrees with our extended molecular data set, where we find that molecules representing even denser gas, such as N$_2$H$^+$ (1–0) or HCN (10–9), reach a maximum in their integrated emission in SBE. Additionally we find the shock tracer CH$_3$OH peaking in their integrated intensities in SBE. This suggests that maybe weak shocks lead to a higher SFR in the SBE compared to the NBE.

6 We do this also with our $\Sigma_{\text{tracer}}$ map in units of M$_\odot$ yr$^{-1}$ kpc$^{-2}$ to calculate star formation efficiencies of the dense molecular gas (see Eq. (8)).

7 We calculate the uncertainties for these SFR values using the uncertainty 33GHz map and apply the equations as in Section 2.3.2. We then get over a 4″ region a SFR uncertainty of ±1.35 × 10$^{-3}$ M$_\odot$ yr$^{-1}$.

The inner bar ends also differ in their molecular masses, as already noted by Schinnerer et al. (2006). We find in our 150 pc sized apertures using Eq. 8 molecular gas mass surface densities ($\Sigma_{\text{mol}}$) of $\approx$189±0.26 M$_\odot$ pc$^{-2}$ in the NBE and $\Sigma_{\text{mol}}$ $\approx$236±5.9 M$_\odot$ pc$^{-2}$ in the SBE. We find that the bar ends have a molecular gas depletion time ($\tau_{\text{depl},150pc}^{\text{mol}}$) that is a factor of 10 higher than NUC; the highest in the SBE $\tau_{\text{depl},150pc}^{\text{mol}}$ $\approx$ 3.05 × 10$^7$ yr (which is rather short, see discussion below).

Towards the NUC we find that stars are formed at a rate of 0.089 M$_\odot$ yr$^{-1}$ over the past ~10 Myr which translates into 0.89 × 10$^8$ M$_\odot$ of recently formed stars. We find $\Sigma_{\text{mol}}$ $\approx$298±1.98 M$_\odot$ pc$^{-2}$ and at the current SFR it will take 0.343 × 10$^7$ years to deplete the present supply of molecular gas. This is shorter (factor of ~10$^2$) than found by previous studies on ~kpc scales, for example a median $\Sigma_{\text{mol}}$ $\approx$2.2 Gyr for the HERACLES galaxies in Leroy et al. (2013), or 1.1 Gyr in Usero et al. (2015). These studies used a Milky Way-like $\alpha_{\odot}$ value (a factor of 10 smaller), which is however, not applicable for NGC 6946 (see e.g. Sandstrom et al. 2013; Bigiel et al. 2020 and Section 2.3.3). The bar ends have a depletion time of a factor of 10 higher than NUC, and if we calculate $\tau_{\text{depl},150pc}^{\text{mol}}$ with a MW value, we would also get into the Gyr range for the bar ends (i.e. $\approx$ 1.6 Gyr for NBE and $\approx$ 3.3 Gyr for SBE). This demonstrates the importance of adopting a proper $\alpha_{\odot}$ factor. The nuclear region of NGC 6946 was studied in terms of its SFR by e.g. Meier & Turner (2004), Schinnerer et al. (2007) and Tsai et al. (2013) using different SFR indicators over different spatial scales.

For example, Schinnerer et al. (2007) found within a 3″$\times$3″ square box region a SFR of ~0.18 M$_\odot$ yr$^{-1}$ using Pa$\alpha$, 6 cm and 3 mm continuum as SFR tracers. We find with our 33 GHz based star formation in the same region a SFR of ~0.11 M$_\odot$ yr$^{-1}$, that is slightly lower than that of Schinnerer et al. (2007).

We remind the reader that the SFR we calculate is based on free-free emission, which is not subject to the extinction problems that complicate the estimation of SFR at optical and ultraviolet wavelengths. The free-free emission is a tracer of high-mass star formation, as it is only sensitive to stars that are able to ionise the surrounding gas and produce an H$\alpha$ region. However, we have to mention some uncertainties with this SFR. A different choice of initial mass function, or stellar population models during the calibration of 33 GHz (see Section 2.3.2), could introduce a systematic offset in the derived SFR but this should not vary from region to region. The parameter $\tau_{\text{SFR}}$ in Eq. (4) has an impact of at most ~7% on the SFR and regional variations in the thermal fraction, $f_T$, are likely to be too small to explain the observed variations in SFR among the bar ends (see e.g. Section 4.1 in Querejeta et al. 2019). Another factor that could potentially vary from region to region is the escape fraction of ionising photons (i.e. which part is absorbed in a region outside the 150 pc aperture and therefore does not contribute to the observed free-free emission). However, these uncertainties probably do not explain the factor of 2 higher SFR in the SBE than in the NBE.

8 Recall that the approximate age sensitivity of the thermal fraction of the 33 GHz continuum emission as a SFR tracer is ~10 Myr.

9 They adopted a distance of 5.5 Mpc to NGC 6946 for their SFR calculations. We have re-scaled their value to the distance of 7.7 Mpc using a factor of 1.8, see Section A.1.

As well as any potential stochasticity due to IMF sampling.
5. Results - Line ratios and relationships among molecular species

Molecular line ratios open up the possibility to investigate the physical and chemical state of the ISM. Integrated line ratios among certain molecules were proposed to provide insights into the environment (e.g. HCO+/HCN; Loenen et al. 2008), the temperatures (HCN/HNC; Hacar et al. 2020) and density variations (e.g. line ratio pattern to CO; Leroy et al. 2017). The question can be asked whether we see differences between the inner bar ends and the nuclear region, and if these line ratio diagnostics hold for an extragalactic extreme environment like the centre of NGC 6946. For a meaningful analysis of the line ratios and their relationships, we need to correct the interferometric data for missing short-spacing information. Therefore, we use the five emission lines (CO (1-0), CO (2-1), HCN, HCO$^+$ and HNC) for which single-dish observations were available (see Table 4). The line ratios are calculated from integrated line intensities in units of K km s$^{-1}$ throughout the entire paper and we refer to them simply as ‘line ratio’.

5.1. Ratios of integrated intensities

In Fig. 5 we show line ratio maps for our SSC + u-v trim data set (see Table 4). We specify the line ratios such that the generally brighter line in the denominator, while the overall weaker line is in the numerator. The line ratio maps were calculated by only taking integrated intensities with S/N > 5 for the fainter dense gas tracers (DGTs: HCN, HCO$^+$ and HNC) and S/N > 15 for the bulk molecular gas tracers (CO); non-detections were discarded from the line ratio maps:

\[
\text{Ratio map} = \frac{I_{\text{line1}}}{I_{\text{line2}}} \left[ \frac{I_{\text{line1}}/\sigma_{\text{line1}} > \epsilon}{I_{\text{line2}}/\sigma_{\text{line2}} > \epsilon} \right] \begin{cases} \epsilon = 5 & \text{for DGTs,} \\ \epsilon = 15 & \text{for CO.} \end{cases}
\]  

(10)

In the next section, we include non-detections in our analysis. For the case of no significant detection we replaced the values with the upper limits (2\(\sigma\) in Eq. 2) and include the propagated errors (\(\sigma_{\text{prop}}\)). We derive them as:

\[
\sigma_{\text{prop}} = I_{\text{line1}} \left[ \frac{\sigma_{\text{line1}}^2}{I_{\text{line1}}} + \frac{\sigma_{\text{line2}}^2}{I_{\text{line2}}} \right]^{1/2}.
\]  

(11)

The errors are expressed on a logarithmic scale of base 10 as:

\[
\sigma_{\log} = \frac{1}{\ln(10)} \times \left( \sigma_{\text{prop}}/I_{\text{ratio}} \right) \approx 0.434 \times \left( \sigma_{\text{prop}}/I_{\text{ratio}} \right).
\]  

(12)

In Fig. 5 the line ratio maps for the central 20$''$ \(\approx 750\) pc show differences in line ratios between the environments NUC, SBE and NBE. In the following we report straight mean values over these regions by applying the mask in Fig. 4. The ratios HCO$^+$/HCN and HNC/HCN both show values below unity in all three regions; and over the entire field of view. In both cases, the ratio to HCN is greater in the NUC than in the SBE or NBE.

Looking at the NUC reveals values of 0.81 ± 0.01 and 0.37±0.01 for HCO$^+$/HCN and HNC/HCN, respectively. Ratios to CO indicate higher values in the SBE than in NBE; best visible in the case of HNC/CO (2-1). We discuss the implications of these line ratios in Section 6.2, 6.3 and 6.4.

5.2. The relationship between molecular lines and SFR surface density

In this section we investigate how our molecular species correlate with \(\Sigma_{\text{SFR}}\) and how the dense gas fraction traced by HCN/CO (we investigate also HCO$^+$/CO and HNC/CO) responds to the integrated intensity of CO (an indicator of the mean volume density, see below). We study how these quantities relate to conditions in the centre of NGC 6946. Fig. 6 shows the relationships we investigate.

We characterise scaling relations by including upper limits and measurement errors, using the hierarchical Bayesian method described in Kelly (2007). This approach is available as a python package: limmix\footnote{https://limmix.readthedocs.io/en/latest/index.html}. It performs a linear regression of y on x while having measurement errors in both variables and being
We specify the covariance between the measurement errors in x and y (\(x_{\text{ycov}}\) parameter) and set \(K\) where

\[ \text{Table 6.} \]

| \(\beta\) slope | \(\alpha\) intercept | \(\rho\) Pearson | \(\rho\)-value | scatter | Cov(\(\log(x),\log(y)\)) |
|-----------------|----------------------|----------------|-------------|---------|--------------------------|
| \(\Sigma_{\text{SFR}}\) | HCN | 1.81±0.13 | -2.52±0.20 | 0.93±6.6E-04 | 9.84E-29 | 0.04 | 9.75 |
| \(\Sigma_{\text{SFR}}\) | HCO+ | 1.55±0.11 | -1.9±0.15 | 0.95±1.7E-02 | 5.10E-19 | 0.04 | 8.24 |
| \(\Sigma_{\text{SFR}}\) | HNC | 1.52±0.14 | -1.33±0.14 | 0.93±1.1E-02 | 1.40E-18 | 0.07 | 3.30 |
| \(\Sigma_{\text{SFR}}\) | CO(1-0) | 2.46±0.22 | -6.56±0.60 | 0.89±2.2E-03 | 7.90E-23 | 0.06 | 112.00 |
| \(\Sigma_{\text{SFR}}\) | CO(2-1) | 1.93±0.22 | -4.68±0.54 | 0.80±2.4E-03 | 5.90E-16 | 0.09 | 68.70 |

HCN / CO(2-1) \(\propto f_{\text{dense}}\) \(\Sigma_{\text{SFR}}\) | CO(2-1) | 0.23±0.06 | -1.63±0.16 | 0.39±3.4E-04 | 5.07E-04 | 0.01 | 0.01 |
| HCO+ / CO(2-1) \(\propto f_{\text{dense}}\) | CO(2-1) | 0.44±0.11 | -2.32±0.26 | 0.45±6.5E-04 | 7.68E-04 | 0.03 | 0.02 |
| HNC / CO(2-1) \(\propto f_{\text{dense}}\) | CO(2-1) | 0.76±0.13 | -3.49±0.31 | 0.66±8.5E-08 | 3.63E-10 | 0.03 | 0.04 |

\(\Sigma_{\text{SFR}}/\) HCN \(\propto f_{\text{dense}}\) \(\Sigma_{\text{SFR}}\) | CO(2-1) | 0.80±0.22 | -3.24±0.56 | 0.64±2.9E-01 | 1.10E-07 | 0.04 | 0.04 |
| \(\Sigma_{\text{SFR}}/\) HCO+ \(\propto f_{\text{dense}}\) | CO(2-1) | 0.60±0.20 | -2.61±0.52 | 0.54±3.2E-01 | 4.59E-04 | 0.04 | 0.03 |
| \(\Sigma_{\text{SFR}}/\) HNC \(\propto f_{\text{dense}}\) | CO(2-1) | 0.51±0.24 | -2.03±0.62 | 0.42±2.8E-01 | 1.17E-01 | 0.05 | 0.02 |

Notes: (1): We perform a Monte Carlo analysis perturbing the x and y data points to get the uncertainty of \(\rho\); (2): The regression intrinsic scatter; able to account for non-detections (upper limits) in y. The regression assumes a linear relationship in the form of:

\[
\log(y) = \beta \times \log(x) + \alpha , \tag{13}
\]

where \(\beta\) is the slope, and \(\alpha\) is the y-intercept\(^\text{12}\). We find Pearson’s correlation coefficients of the data sets for each fitted relationship, and the 3\(\sigma\) confidence intervals are estimated via Markov chain Monte Carlo (MCMC). For a detailed description we refer to Kelly (2007). We provide all the correlations in Table 6.

Dense molecular gas traced by, e.g., HCN emission, has been observed to correlate with SFR (e.g. Gao & Solomon 2004; Lada et al. 2010, 2012). Kauffmann et al. (2017) showed that HCN traces more extended gas and therefore can have an impact on the observed SF trends in galaxies (also see e.g. Pety et al. 2017; Barnes et al. 2020b). Krumholz & Thompson (2007) showed that star formation correlates with any line with a critical density comparable to the median molecular cloud density. Therefore, we expect to see positive correlations between \(\Sigma_{\text{SFR}}\) and the surface density of HCN, HCO+ and HNC. In our observations this is confirmed with the additional characteristic that the molecular line with the lowest effective critical density (\(n_{\text{eff}}\)) shows the strongest correlation (\(n_{\text{eff}}\) ordered as HCO+ < HNC < HCN; see Table 2). HCO+ shows the strongest (\(\rho < 0.95\), see Table 6 for uncertainties of \(\rho\)) correlation with a slope of \(\beta = 1.55\) and a small intrinsic scatter:

\[
\log(\Sigma_{\text{SFR}}) = 1.55 \pm 0.11 \times \log(I_{\text{HCO}+}) - 1.91 \pm 0.15 . \tag{14}
\]

We note that our slopes are all higher (\(\beta > 1\)) than those found at global scales (\(\beta < 1\); e.g. Gao & Solomon 2004; Krumholz & Thompson 2007). We speculate that this is due to two contributing factors. Firstly, in this work we are focussing on the central 20′′ ≈ 745 pc, and not the whole galaxy disc. Hence, this could be due to the limited dynamic range in environmental conditions we are including within the analysis - that is focussing on the densest and most actively star-forming gas within the galaxy. Secondly, this could be a result of the resolution obtained with our PdBI observations. At around 150 pc, we are close to resolving individual discrete star-forming and/or quiescent regions, which could result in the different slope compared to lower resolution studies that include an average on small scale conditions within each sample point; somewhat akin to following a branch of the tuning fork within the recent ‘uncertainty principle for star formation’ framework (Krujissjen et al. 2018, 2019; Chevance et al. 2020a; Kim et al. 2021). The dense gas fraction, \(f_{\text{dense}}\), is usually traced by the integrated intensity of HCN (1–0) over CO, has been observed to increase towards the centres of galaxies (e.g. Usero et al. 2015; Bigiel et al. 2016; Gallagher et al. 2018b; Jiménez-Donaire et al. 2019; Jiang et al. 2020; Bešlić et al. 2021). In turbulent cloud models, increasing the mean volume density of a molecular cloud results in a shift of the gas density distribution to higher densities (e.g. Federrath & Klessen 2013). In addition, the velocity dispersion (or Mach number) widens the density PDF, which causes a larger fraction of the mass to be at higher gas densities. Combined, these increase the fraction of gas above a fixed density (e.g. the effective critical density of HCN), and consequently, these models predict a positive correlation between the volume density and \(f_{\text{dense}}\) (see Padoan et al. 2014 for a review). Such trends are, in particular, interesting to study within galaxies centres environments thanks to their higher average densities and broader (cloud-scale) line widths compared to typical disc star-forming regions (e.g. Henshaw et al. 2016; Krieger et al. 2020). In the following we use the integrated intensity of CO (2–1) as an indicator of the mean volume density (Leroy et al. 2016; Sun et al. 2018; Gallagher et al. 2018a, see also Section 6.4) and explore the dense gas fraction using HCN, HCO+ and HNC. All three \(f_{\text{dense}}\) versus CO (2–1) fits in Fig. 6 present sub-linear power-law indices (i.e. \(\beta < 1\)). We find that the correlations are weakest for the dense gas fraction using HCN (\(\rho < 0.39\)) and strongest for HNC / CO (2–1) (\(\rho < 0.66\)):

\[
\log\left(\frac{I_{\text{HNC}}}{I_{\text{CO}(2-1)}}\right) = 0.76 \pm 0.13 \times \log\left(\frac{I_{\text{CO}(2-1)}}{I_{\text{CO}(1-0)}}\right) - 1.63 \pm 0.16 . \tag{15}
\]

The particular order in the slopes and correlation coefficients do not follow the order of \(\text{metal}\) as given in Shirley (2015). Instead, they show the order of \(\rho_{\text{HNC}} > \rho_{\text{HCO}+} > \rho_{\text{HCN}}\) (see second row in Fig. 6). Possible explanations for this behaviour could be anomalous excitation for one of the species, for example IR pumping of HCN and HNC levels and/or peculiar filling factors. The star

\(^{12}\) We specify the covariance between the measurement errors in x and y (\(x_{\text{ycov}}\) parameter) and set \(K = 2\).

\(^{13}\) In this work, we take the CO (2–1) data for our \(f_{\text{dense}}\) estimates because they have a higher S/N and better quality than CO (1–0).
the overdense, star-forming gas; in effect reducing the apparent SFE. From that we would expect to see SFE$^\text{dense}$ to drop with $I_{\text{CO}(2-1)}$ ($\propto$ volume density) as it has been observed over the disc regions of galaxies (e.g. Gallagher et al. 2018b; Jiménez-Donaire et al. 2019). We use the ratio of $\Sigma_{\text{SFR}}$ to the integrated intensities of the dense gas tracers as SFE$^\text{dense}$, and find a different picture of SFE$^\text{dense}$ with galactocentric radius – increasing towards the NUC; as it shows higher efficiencies in the NUC than in the bar ends (see third row in Fig. 6). We find a moderate\(^{14}\), approximately linear correlation between $\Sigma_{\text{SFR}}/I_{\text{HCN}}$ and $I_{\text{CO}(2-1)}$. The other two SFE$^\text{dense}$ measurements show weak sub-linear relationships with $\rho \sim 0.46$ and $\rho \sim 0.19$ for ratios using HCO$^+$ and HNC, respectively. We find that SFE$^\text{dense}$ increases with increasing $I_{\text{CO}(2-1)}$, contrary to the trends found by Gallagher et al. (2018b): Jiménez-Donaire et al. (2019). The reason for that could be the special environment of NGC 6946 (inner bar) and/or the different used SFR tracers (we use the free-free emission of 33 GHz continuum compared to Hα+$24\mu$m and total infrared). Also the above studies could not resolve the inner bar of NGC 6946 (Jiménez-Donaire et al. 2019, angular resolution of $33'' \approx 1$ kpc) or NGC 6946 was not in the nearby disc galaxy sample (Gallagher et al. 2018b). However, we notice, as expected, that stronger correlations in $I_{\text{dense}}$ result in weaker correlations in SFE$^\text{dense}$ and vice versa (e.g. $I_{\text{HCN}}$/$I_{\text{CO}(2-1)}$ with $\rho = 0.76 \pm 0.13$ and $\Sigma_{\text{SFR}}/I_{\text{HNC}}$ with $\rho = 0.51 \pm 0.24$; see Table 6).

6. Implications for spectroscopic studies of other galaxies – from bulk molecular gas to dense gas

Here we discuss some of the common integrated line ratios in more detail and what they can be used for. We compare our high-resolution (150 pc) integrated line ratios of dense gas tracers towards the central region of NGC 6946 with available dense gas tracers from the EMPIRE survey, which include eight additional galaxy centers. It is worth noting that the central regions in the EMPIRE sample are $\sim 1$ kpc sized areas which result in one data point per galaxy (see Jiménez-Donaire et al. 2019 for more details). Nevertheless, it provides us with an understanding of how NGC 6946 compares to other centers.

6.1. $R_{21}$ variations in the nuclear region and inner bar ends

The CO (2–1)-to-CO (1–0) line ratio, $R_{21}$, is widely used to convert CO (2–1) emission to CO (1–0), which then can be further converted via the $\alpha_{\text{CO}}$ conversion factor to the molecular gas mass. It has been shown that higher $R_{21}$ values are expected within the central kpc in individual galaxies (Leroy et al. 2009, 2013; Koda et al. 2020). The same trend has been found by den Brok et al. (2021) and Yajima et al. (2021) studying a galaxy sample. NGC 6946 is in both of the aforementioned studies. They find within the central kpc region $R_{21} < 0.7$ (at an angular resolution of $33'' \sim 1$ kpc; den Brok et al. 2021 using the EMPIRE sample) and $R_{21} \sim 1.1$ (angular resolution of $17'' \sim 0.6$ kpc; Yajima et al. 2021). However, these studies are not able to resolve variations within the centre between different sub-features. From a physical point of view, $R_{21}$ should depend on the temperature and density of the gas, as well as on the optical depths of the lines (e.g. Peñaloza et al. 2018). Therefore, understanding how $R_{21}$ varies in response to the local environment also has the prospect of providing information about the physical conditions of the molecular gas.

\(^{14}\) Here we refer to a moderate correlation if $\rho$ lies in the range of 0.5–0.7.
With our higher resolution ($4'' \approx 150$ pc) observations we are able to resolve smaller-scale structures and thus have the opportunity to investigate variations of $R_{21}$ within the centre. In Fig. 7 we show $R_{21}$ against galactocentric radius, highlighting NUC, NBE and SBE in different colours.

We see along the galactocentric radius, in the centre higher $R_{21}$ values, an initial steady decrease followed by a gradual increase. We find average $R_{21}$ of $0.65 \pm 2E^{-3}$ within NUC and even lower values in the southern end of the bar $R_{21} = 0.62 \pm 3E^{-2}$ (see Table 7). Interestingly, however, we observe higher $R_{21}$ values towards the northern end of the bar ($R_{21} = 0.70 \pm 3E^{-2}$) compared to the NUC (factor of $\sim 1.08$), despite the higher $\Sigma_{\text{SFR}}$ in the SBE compared to the NBE (see Section 4). The reason for a higher $R_{21}$ value could be related to denser gas and/or warmer gas with higher temperatures. We colour-code points in Fig. 7 by their HCN ($1-0$)/CO ($2-1$) line ratio ($\propto f_{\text{dense}}$) and find them showing higher $f_{\text{dense}}$ towards the NUC. Furthermore, we would expect to observe higher HCN-to-CO ratios towards the NBE. However, we do not see an increase in the denser gas in the NBE, suggesting a different physical driver for the increased $R_{21}$ in the

---

**Fig. 6. Correlation plots ordered by their slope, $\beta$.** Dark purple colours show HCN, purple HCO$^+$ and pink HNC. Top row: Integrated intensities of the dense gas tracers (ordered by their slope, $\beta$) versus $\Sigma_{\text{SFR}}$. Middle row: Integrated intensity of CO ($2-1$) – an indicator of the mean volume density – versus the line ratio with CO ($2-1$) – a spectroscopic tracers of $f_{\text{dense}}$; Bottom row: Integrated intensity of CO ($2-1$) – an indicator of the mean volume density – versus the ratio of $\Sigma_{\text{SFR}}$ with the dense gas tracers – a spectroscopic tracers of SFE$_{\text{dense}}$. The `linmix` fits (accounting for upper limits) are shown as solid lines surrounded by $3\sigma$ confidence intervals (shaded regions of corresponding colours). Absolute uncertainties are plotted on each data point, which are generally small towards the regions NUC, NBE and SBE. We find the highest uncertainties in the outskirts in our $\Sigma_{\text{SFR}}$ map. Correlations including HNC result in 58 significant sight lines and 15 upper limits (denoted as light pink markers). We display in each panel Pearson’s correlation coefficient and the power-law slope, intercept and $p$-value (see Table 6).
NBE. We analyse the three regions regarding their molecular gas density in more detail in Section 6.4.

In summary, we find higher $R_{21}$ values towards one of the inner bar ends of NGC 6946 compared to the nuclear region. If substructures such as small-scale bar ends are to be observed and analysed, $R_{21}$ may possibly deviate in a minimal way from the kpc-sized $R_{21}$ values from the literature.

![Image](https://example.com/image.png)

**Fig. 7. $R_{21}$ against galactocentric radius.** The circular shaped markers represent all of the $R_{21}$ values for the central 20$^\prime\prime$ = 745 pc coloured by their $T_{\text{dust}}$. The different sizes show their varying signal-to-noise ratios in CO (2-1). Additionally, we overplot the contours of the three different regions: The cyan colour refers to the nuclear region (NUC), the green to the northern bar end (NBE) and the magenta to the southern bar end (SBE). Along the galactocentric radius, we find in the centre higher $R_{21}$ values, an initial steady decrease followed by a gradual increase. $R_{21}$ towards NBE is higher than expected (more in Section 6.1).

6.2. HNC/HCN: sensitive to kinetic temperatures in extragalactic environments?

In interstellar space, isotropes do not necessarily share similar chemical or physical properties. HNC (hydrogen iso-cyanide) and HCN (hydrogen cyanide) isotropes are both abundant in cold clouds, but at temperatures exceeding ~30 K, HNC begins to be converted to HCN by reactions with atomic H. These isotropes exhibit an abundance ratio of unity at low temperatures (Schilke et al. 1992; Graninger et al. 2014). A major study to understand this ratio, which was focused on the galactic SF region Orion Molecular Cloud 1 (OMC-1), was carried out by Schilke et al. (1992). They found that the HNC/HCN ratio is ~1/80 in the direction of Orion Kleinmann-Low (Orion-KL) but increases to 1/5 in regions with lower temperatures near Orion-KL. In the coldest OMC-1 regions, the ratio rises further to 1. The temperature dependence suggests that the ratio must be kinetically controlled (Herbst et al. 2000), so that the integrated intensity line ratio HNC/HCN should decrease at higher temperatures (Pety et al. 2017).

Whether this ratio is sensitive to temperatures in extragalactic sources is uncertain (e.g. Aalto et al. 2002; Meier & Turner 2005, 2012). For example, Meier & Turner (2005) found a kinetic temperature for the centre of IC 342 using the HCN/HNC ratio and the empirical relation of Hirota et al. (1998) of a factor of 2 less than the dust temperature and the kinetic temperature of the gas using CO (2-1) and ammonia (NH$_3$). They suggested that there might be an abundant dense component in IC 342 that is significantly cooler and more uniform than the more diffuse CO, but this was not consistent with the similar distribution of CO, HNC and HCN, unless such a dense component directly follows the diffuse gas. Alternatively, they assumed that this line relationship might not capture temperature, for the nuclear region of IC 342. Also Aalto et al. (2002) find overluminous HNC in many of the most extreme (and presumably warm) (U)LIRGs and suggest that its bright emission cannot be explained by the cool temperatures demanded.

Recently, however, this line ratio has come back into focus. Hacar et al. (2020) demonstrated the strong sensitivity of the HNC/HCN ratio to the gas kinetic temperature, $T_k$, again towards the Orion star-forming region. They compared the line ratio with NH$_3$ observations (Friesen et al. 2017) and derived $T_k$ from their lower inversion transition ratio NH$_3$ (1,1)/NH$_3$ (2,2). In particular, they found that $T_k$ can be described by a two-part linear function for two conditions (we show only Eq. (3) in Hacar et al. 2020):

$$T_k [K] = 10 \times \frac{I_{\text{HCN}}}{I_{\text{HNC}}} \quad \text{for} \quad \frac{I_{\text{HCN}}}{I_{\text{HNC}}} \leq 4.$$  

However, since the NH$_3$ (1,1)/NH$_3$ (2,2) transitions are only sensitive to $T_k$ $\leq$ 50 K (see e.g. Fig. 1 of Mangum et al. 2013), the calibration shown above only represents the low temperature regime. The challenge of apply such concepts in nearby galaxies is that the concentrations of dense gas studied by Hacar et al. (2020) in the local Milky Way environment (i.e. Orion) are very compact (~0.1–1 pc; Lada & Lada 2003), and representative of solar neighbourhood environmental conditions (e.g. chemistry, and average densities, Mach numbers and kinetic temperatures). Achieving such a resolution is currently extremely difficult in an extragalactic context (e.g. 1 pc = 0.025$''$ at the distance of the NGC 6946), potentially limiting our capability to determine kinetic temperatures (e.g. when using H$_2$CO; see Mangum et al. 2019 and below). That said, galaxy centres present an ideal regime in which to focus our efforts. As densities similar to the concentrations observed within local star-forming regions are not compact, but can span (nearly) the entire CMZ (so up to 100 pc), leading to luminous and, importantly, extended HCN and HNC emission (Longmore et al. 2013; Rathborne et al. 2015; Krieger et al. 2017; Petkova et al. 2021). Hence, testing this temperature probe within galaxy centres overcomes the requirement for such extremely high-resolution observations, and should be possible with $\sim$ 100 pc scale measurements presented in this work.

We find in the nuclear region of NGC 6946 a mean HCN/HNC ratio of ~0.37. For the bar ends we find lower ratios: ~0.31 for NBE and ~0.32 for the SBE (see Table 7). Jiménez-Donaire et al. (2019) reported over kpc-scales a ratio of ~0.31. There are no other ratios of HNC and HCN in the literature for a comparison, since HNC has barely been observed towards NGC 6946. If we assume that the ratio of HCN and HNC traces kinetic temperature and adopts the Hacar et al. (2020) relation\footnote{The equation in Hacar et al. 2020 uses HCN over HNC (HCN/HNC), therefore we have for e.g. NUC = 1/0.37 = 2.7.}, then we would infer a $T_k$ (HCN/HNC) of ~27 K for the NUC. For the bar ends we calculate slightly higher temperatures of ~31 K and ~32 K (on 4$''$ $\approx$ 150 pc scales). Meier & Turner (2004) predict $T_k$ ~20–40 K (for $n_{\text{H}_2}$ = 10$^3$ cm$^{-3}$) based on CO and its isotopologues using a large velocity gradient (LVG) radiative transfer model (building on the models presented in Meier et al. 2000). Including HCN...
into their LVG models, favoured higher $T_k$ ($\sim$90 K) and $n_{HI}$ ($\sim 10^4 - 10^5 \text{ cm}^{-3}$), but these numbers are sensitive to whether $^{13}$CO and HCN trace the same gas component. With the inverse transition of NH$_3$, Mangum et al. (2013) found $T_k$ = 47$^\pm$8 K (using the NH$_3$ (1,1)/NH$_3$ (2,2) ratio) which is a factor of $\sim$2 higher than our inferred $T_k$ (HNC/HCN). The higher excitation NH$_3$ (2,2)/NH$_3$ (4,4) ratio, which monitors $T_k \lesssim 150$ K, was not yet detected towards NGC 6946 (Mangum et al. 2013; Gorski et al. 2018). Those studies already showed that an unambiguous determination of the kinetic temperature is challenging.

Comparing our obtained $T_k$ (HNC/HCN) to typical $T_k$ measurements towards the central molecular zone (CMZ) in the Milky Way, reveals higher gas temperatures in the CMZ ($T_k > 40$ K; Ao et al. 2013; Ott et al. 2014; Ginsburg et al. 2016; Milkey Way, reveals higher gas temperatures in the CMZ (Krieger et al. 2017). Investigating individual CMZ clouds, Ginsburg et al. (2016) used para-H$_2$CO transitions as a temperature tracer which is sensitive to warmer ($T_k > 20$ K) and denser ($n \sim 10^4$ cm$^{-3}$) gas. They determined gas temperatures ranging from $\sim$60 to $\sim$100 K. We know from extragalactic studies that high kinetic temperatures ($50 \sim 250$ K) can be produced by both cosmic ray and mechanical (turbulent) heating processes (Mangum et al. 2013; Gorski et al. 2018). The CMZ of our own Galaxy seems to be different in this respect where the mismatch between dust and gas temperature at moderately high density ($n \sim 10^4$ cm$^{-3}$) is better explained by mechanical heating (Ginsburg et al. 2016). However, it is not clear what might be the reason for observing low $T_k$ in an environment where we expect mechanical heating processes.

Compared to the better studied extragalactic nuclear source NGC 253, Mangum et al. (2019) found kinetic temperatures on $5'' \approx 85$ pc scales of $T_k > 50$ K using ten transitions of H$_2$CO, while on scales $<1''$ ($\sim 17$ pc) they measure $T_k > 300$ K. Using NH$_3$ as a thermometer indicates the presence of a warm and hot component with $T_k = 75$ K and $T_k > 150$ K, respectively (Gorski et al. 2018; Pérez-Beaupuits et al. 2018). The reported HCN/HNC ratio over the whole nucleus is $\sim$1, which if Hacar et al. (2020) were true would imply $T_k$(HNC/HCN) $\sim$10 K. This is in contrast to the aforementioned warm component a factor of 7 lower. It indicates that this ratio provides no reliable information about $T_k$ in the extragalactic region of NGC 253.

We find for the eight kpc-sized galaxy centers in the EMPIRE sample – using Eq. (16) $- T_k$ (HNC/HCN) lower than 50 K for almost all galaxies.16 NGC 3627 and NGC 5055 exhibit higher kinetic temperatures, 58 K and 61 K, respectively. Bešlić et al. (2021) found towards NGC 3627 on 100 pc scales (using the same framework) lower $T_k$ (HNC/HCN) of $\sim$34 K.

In summary, the HNC/HCN ratio results in low inferred kinetic temperatures in galaxy centres ($T_k < 50$ K) if Hacar et al. (2020) prescription can be applied. However, in the absence of other accurate kinetic temperature measurements (with NH$_3$ or H$_2$CO) against NGC 6946 and the EMPIRE galaxies, we speculate that the isomer ratio is not a suitable $T_k$ probe for large sized extragalactic regions, and, in particular, towards galaxy centres that can also have high optical depths and complex chemistry (also AGN activity and prominent additional excitation mechanisms). A comparison with similarly high resolution observations towards a galaxy centre using kinetic temperatures derived from ammonia emission would be worthwhile to further investigate the HNC/HCN temperature sensitivity framework of Hacar et al. (2020).

6.3. Examining ratios among HCN, HCO$^+$ and HNC as a diagnostic of AGN state

Clouds of gas in the inner kpc of galaxies are exposed to intense radiation, which can emanate from an active galactic nucleus (AGN), seen as hard X-rays with $E > 1$ keV; from starburst regions, dominated by radiation of O and B stars; or from both. Excess of X-ray emission affects the thermal and chemical balance of the surrounding ISM, which in turn could influence molecular line emission (see below). The centre of NGC 6946 exhibits no clear indication for the presence of an AGN. Holt et al. (2003) studied the distribution of the X-ray emission over the full disc of NGC 6946 and found several low-luminosity point-like sources, one of which coincides with the dynamical centre determined by Schinnerer et al. (2006).

Theoretical modelling of ratios between HCO$^+$ and HCN suggested it as a diagnostic tool to distinguish between photon-dominated regions (PDRs) and X-ray-dominated regions (XDRs) for a given column density of $N \sim 10^{23}$ cm$^{-2}$ in the presence of ionizing radiation (Meijerink & Spaans 2005; Meijerink et al. 2007). In their models the HCO$^+$/HCN ratio seems to systematically vary with gas density, the incident ultraviolet and infrared radiation field. Also mechanical heating and cosmic ray ionization could be possible sources of variations in HCO$^+$/HCN (Bayet et al. 2010; Meijerink et al. 2011). Including HNC to the analyses, Loenen et al. (2008) claims that in XDRs HNC is always stronger than the HCN line, whereas the inverse trend is seen in PDRs (resulting in line ratios lower than unity). For their analyses they used observations obtained with the IRAM 30-m telescope for the HCN, HNC, HCO$^+$ line emission of 37 infrared luminous galaxies (Baan et al. 2008) and additional 80 sources from the literature (see Loenen et al. 2008 and references therein); all unresolved measurements. Then they compared the observational data with the predictions of PDR and XDR models (Meijerink et al. 2007) with varying volume densities, ranging from $10^3$ to $10^6$ cm$^{-3}$.

A low HCO$^+$/HCN ratio was proposed as the signature of an AGN. Since studies of galaxies hosting an AGN have found evidence for enhanced emission from HCN, relative to HCO$^+$ (e.g. Kohn et al. 2001; Imanishi et al. 2007; Davies et al. 2012). Recently, however, this statement has been under discussion, for example; in Privon et al. (2020). They investigated NuSTAR hard X-ray emission together with literature HCO$^+$ and HCN observations and found no correlation between the HCO$^+$/HCN ratio and the X-ray to IR luminosity ratio or the AGN luminosity. Thus, observing enhanced HCN relative to HCO$^+$ against a galaxy centre is not convincingly linked to currently observed AGN activity.

We now apply the PDR versus XDR framework by Baan et al. (2008) and Loenen et al. (2008) to our observed dense gas tracers towards the centre of NGC 6946 and investigate Chandra X-ray observations.

We see from the top panels of Fig. 5 that the HCO$^+$/HCN and HNC/HCN ratios exhibit values lower than unity in all three regions (see Table 7). In Fig. 8 we investigate the diagnostic plots proposed by Baan et al. (2008) and Loenen et al. (2008) to visually discriminate between XDR and PDR by comparing the line ratios between HCO$^+$, HCN and HNC in the central 20$''$ of 745 pc towards NGC 6946. In all these diagnostic plots (panels a–d), NGC 6946 is in the PDR regime. Panel (d) could indicate a linear relationship between HNC/HCN and HNC/HCO$^+$. We see log$_{10}$(HNC/HCN) in the range of $\sim$0.80 to $\sim$0.25 and log$_{10}$(HNC/HCO$^+$) between $\sim$0.70 and $\sim$0.10. We investigate which mechanism could cause the observed ranges of line ra-

---

16 For NGC 3627, NGC 4254 and NGC 5055 we had to take for the calibration the second part of the two-part linear function in Hacar et al. (2020).
For NGC 6946 – as mentioned above – there is no clear evidence for an AGN. In the following we investigate whether there are X-ray sources that are strong enough to trigger an XDR, although the diagnostic diagrams favour a PDR. The *Chandra* X-ray map (0.5–7.0 keV) in counts towards the central 20″ of NGC 6946 shows us that most of the diffuse X-ray emission is coming from a region not associated with the NUC, SBE and NBE (see Fig. 8). The stronger of the two detected X-ray sources near NUC by *Holt et al.* (2003) (shown as black crosses) is ~2″ away from the dynamical center position (shown as red circle). They find a flux of $2.8 \times 10^{-13}$ erg s$^{-1}$ cm$^{-2}$ and classified its hardness as ‘medium’ (see their Table 2 for SourceID 45). Scaling this flux to our working resolution results in $4.53 \times 10^{-13}$ erg s$^{-1}$ cm$^{-2}$. This is similar to the lowest values in *Meijerink et al.* (2007). This suggests that the brightest X-ray source might affect the gas within a beam scale, but hardly beyond that.

---

$G_0 = 10^2$ and $G_0 = 10^5$ are the default minimum and maximum $G_0$ in their model outputs.

---

**Fig. 8. Diagnostic plots using integrated line ratios of HCN, HNC and HCO$^+$ versus each other.** Left panels: (a) Integrated HCO$^+$/HCN versus HNC/HCN$^+$ ratios. (b) Integrated HCO$^+$/HCN versus HNC/HCN ratios. (c) Integrated HNC/HCN versus HNC/HCN$^+$ ratios. The grey dashed lines marks the border between XDR and PDR (*Baan et al.* 2008; *Loenen et al.* 2008). Circles indicate reliable values (S/N > 5) and upper limits for the central 20″ ~ 745 pc towards NGC 6946. Stars show the EMPIRE galaxies and stars with red contours present galaxy centres hosting an AGN (*Goulding & Alexander* 2009). For two of them we find ancillary data: the cross shaped markers show the ~4″ (~ 166 pc) M 51 observations (*Querejeta et al.* 2016) and the ~2″ (~ 100 pc) NGC 3627 observations (*Beljić et al.* 2021); (d): The enclosed integrated HNC/HCN versus HNC/HC$^+$ with the kpc-sized centres of the EMPIRE survey (see *Jiménez-Donaire et al.* 2019 for details). NGC 6946 and the EMPIRE galaxies are in the PDR regime in all panels. Interestingly, EMPIRE galaxies harbouring an AGN do not show an enhancement of HCN as suggested in many studies (see text for a discussion). We run *Meijerink & Spaans 2005* PDR models for the observed ranges of line ratios (blue and red shaded areas) by (i) fixing the radiation field and (ii) fixing the density. The red and blue lines show the model output (more in text). The colours in (a–d) indicate $\Sigma_{\text{SFR}}$. We have normalised them to the mean $\Sigma_{\text{SFR}}$ value and find no trend with the integrated line ratios. Upper right panel: X-ray 0.5–7.0 keV in counts for NGC 6946 with integrated CO (2–1) contours on top. The black crosses mark the positions of the detected X-ray sources by *Holt et al.* (2003) which are not strong enough to trigger a XDR.
Interestingly, all the kpc-sized central regions of the EMPIRE galaxies in Fig. 8 lie in the PDR regime. Their $\log_{10}$(HCN/HCN) ratios are in the same range as those observed for NGC 6946. On the other hand, $\log_{10}$(HCN/HCO$^+$) varies only from $-0.60$ to $-0.20$. The galaxies NGC 3627, NGC 5055 and M51 are known to host an AGN classified as LINER (Goulding & Alexander 2009) and are still located in the PDR regime in Fig. 8. There is no strong enhanced HCN emission relative to HCO$^+$ towards these three galaxy centres which would ‘move’ them to the XDR regime of the diagnostic plots. The fact that they do not lie within the XDR region of Loenen et al. (2008) could be because: a) their models are not quantitatively accurate; b) the EMPIRE AGNs are faint and their effects are diluted when averaging over 1 kpc regions; and c) a different model that does not require the significant variations in the line ratio to be driven by a PDR or XDR (e.g. Viti 2017). We test the dilution effects in a way that we include available high-resolution dense gas observations of M 51 and NGC 3627 (i.e. $\sim 4'' \approx 166$ pc from Querejeta et al. 2016 and $\sim 2'' \approx 100$ pc from Bešlić et al. 2021, respectively; see Section 2.3). For both, we show line ratios for the central beam size; they are all in the PDR regime. From that we speculate that the diagnostic plots shown in Fig. 8 and in particular the HCO$^+$/HCN line ratio might not be a unique indicator to diagnose the presence of an AGN in galaxies on kpc/sub-kpc scales. This finding is consistent with the previous studies by Privon et al. (2020) and Li et al. (2021).

6.4. Density variations at the inner bar ends and nuclear region

Already in Fig. 2 we saw that the CO (1-0) and CO (2-1) emission is spatially more extended than HCN (1-0), HCO$^+$ (1-0) or HNC (1-0), which could be a sign that the CO lines trace a lower density regime. That said, line intensities depend not only on density, but also on optical depth, elemental abundance variations and IR pumping (see e.g. Shirley 2015; Barnes et al. 2020a), and all of these effects can thus drive the relative line intensity ratios.

Leroy et al. (2017) analysed how changes in the sub-beam density distributions affect the beam-averaged line emissivity, by applying non-LTE radiative transfer models coupled with a parametrised density probability distribution. They found that the strength of tracer emission for dense gas is more sensitive to changes in gas density than for example CO. More precisely, the line can still be emitted at densities below the critical density, but with lower efficiency. As a result, a small increase in gas density can significantly increase the efficiency of the emission. This is not the case for lines with a lower critical density (e.g. bulk molecular gas tracer – CO). The density of the gas exceeds the critical density, so varying the gas density does not significantly affect the efficiency of the emission.

We investigate the scenario from Leroy et al. (2017) that line ratios can reflect changes in density distributions. In Figure 9 we investigate the dependence of the observed molecular line ratios. The colourbar shows the integrated intensity of CO (an indicator of the volume density at cloud scales Leroy et al. 2016; Sun et al. 2018) towards the 150 pc sized NUC, NBE and SBE (see Fig. 4; we take the mean over the 7 hexagonal points). The upper panel shows on the y-axis logarithmic molecular line ratios with CO (2-1). At first glance, within NUC we find line ratios being enhanced by at least 20% compared to the inner bar ends. Identifying ratio variations by eye in the two bar ends is challenging. The lower panel shows the relative differences. Here we divide for example HCN/CO by the mean HCN/CO of all the 3 regions. We ordered them by their flaring appearance. We see the trend is not monotonic with $n_{\text{eff}}$, instead they show an order of HCN < HCO$^+$ < HNC, that is the order of decreasing intensity. We find that the highest ratios are associated with NUC (purple marker), except for the CO (1-0)/CO (2-1) ratio. Comparing the two bar ends we find (i) higher ratio values towards the SBE (orange marker) for ratios including CO (1-0) and HCN, (ii) higher ratio values towards the NBE (brown markers) for ratios including HCO$^+$ and HNC and, (iii) that the highest differences between the SBE and NBE is $\sim 10\%$ which are ratios including CO (1-0) and HCO$^+$. The HCO$^+$ intensity in the SBE seems to be under-luminous compared to the other two environments. The HNC intensity provides the largest dynamic range, with the highest value seen in the NUC and the lowest one in the SBE.

We compare the observed line ratios of CO, HCN, HCO$^+$ and HNC in the three regions using radiative transfer models to estimate the mass-weighted mean gas density. From the temperature analyses (see Section 6.2) we would expect potential higher densities in the bar ends, whereas from the R$_2$ examinations (see Section 6.1) we would anticipate higher molecular densities in
the NBE than in the SBE. Furthermore, from our derived $\Sigma_{\text{SFR}}$ (see Section 4 and Table 7) we would expect higher molecular gas densities in the SBE than in the NBE. For that purpose we use the radiative transfer code Dense Gas ToolBox (Puschign 2020) which is based on the approach by Leroy et al. (2017) including that emission lines emerge from an isothermal ensemble of gas densities that follow a log-normal distribution (with or without power-law tail) in combination with RADEX calculations (van der Tak et al. 2007). It works as follows: (i) Using Bayesian inference, model parameters (i.e. temperature and density) are inferred from a number of integrated input line intensities. (ii) The assumed fixed line optical depths and abundances are calibrated through observations of the EMPIRE survey (Jiménez-Donaire et al. 2019, which includes NGC 6946). (iii) Then it solves for line emissivities in each density bin which are calculated using expanding-sphere escape probabilities (large velocity gradient approximation) as implemented in RADEX (van der Tak et al. 2007). (iv) Given the estimated kinetic temperature in Section 6.2, we are assuming a fixed temperature of 30 K. A more detailed description of the Dense Gas ToolBox will be provided in J. Puschign et al. (in prep.). The models suggest that the density in NUC is highest with a mass-weighted mean density of $\sim 10^{4.0}$ cm$^{-3}$, while the lowest one is found in the NBE with a value of $\sim 10^{3.7}$ cm$^{-3}$.

In summary, these models broadly agree with our empirical findings of Fig. 9. The higher mass-weighted mean densities in the SBE agree with the enhanced $\Sigma_{\text{SFR}}$ in the SBE (compared to the NBE). However, the model results do not explain the elevated $R_{21}$ in NBE (see Fig. 7) and, therefore, an additional physical mechanism has to be responsible for it. A note of caution is appropriate, as the mass-weighted mean density differences found among the three regions are of small magnitude and might not be significant in conjunction with the model assumptions (see Table 7). For example, the kinetic temperature in the model is fixed and the same for the two bar ends and the nuclear region. An accurate measurement of kinetic temperatures on parsec scales could unveil the duality of the bar ends.

7. Conclusion

In this paper we present the high-resolution (2′−4′′ ≈ 75−150 pc at 7.7 Mpc distance) IRAM PdBI multi-molecule observation towards the inner 50′′ ≈ 1.9 kpc of the Fireworks Galaxy, NGC 6946 (see Fig. 1). Our compiled data set includes a total of 14 detected molecular lines in the mm-wavelength range. For the analyses in this paper, we convolve our molecular lines to a common beam size of 4′′, and analyse three distinct environmental regions associated with the inner bar of NGC 6946: the nuclear region (NUC), the northern inner bar end (NBE) and the southern inner bar end (SBE) (see Fig. 4 for mask and Table 7).

We find the following results:

1) We report the first detection of C$_{2}$H (1−0), HC$_{3}$N (10−9) and HC$_{5}$N (16−15) towards NGC 6946.

2) The different lines show distinct morphology. More extended emission is seen with CO (1−0), CO (2−1) (associated with bulk molecular gas), HCO$^{+}$ (1−0), HCN (1−0) and HNC (1−0). The latter three are typically used to trace denser gas. We find that even denser gas (e.g. as seen by N$_{2}$H$^{+}$ (1−0)) and shocks (e.g. as seen by CH$_{3}$OH (2−1)) are more concentrated in the SBE than in the NUC or NBE (see Fig. 2).

3) We discover a higher star formation rate (SFR) in the SBE. Shocks and denser gas in this bar end could possibly enhance star formation compared to the lower SFR in NBE.

4) We find among our molecules that HCO$^{+}$ (1−0) correlates best with $\Sigma_{\text{SFR}}$, with Pearson’s correlation coefficient $\rho$ ∼0.95. Additionally, we find a relation of $\rho$ to the effective critical density ($n_{\text{eff}}$) of the dense gas tracers.

5) The dense gas fraction fits do not follow the order of $n_{\text{eff}}$: instead they show the order of $\beta_{\text{HNC}} > \beta_{\text{HCO}} > \beta_{\text{HCN}}$. The strongest correlation among our mean volume density versus different $f_{\text{dense}}$ is ICO(2−1) versus HNC/CO(2−1) with $\rho$ ∼0.76.

6) We find that SFE$_{\text{dense}}$ increases with increasing gas surface density (i.e. ICO(2−1) emission) within the inner ∼ 1 kpc of NGC 6946, contrary to the opposite trends found within low-resolution observations covering the whole disc (Gallagher et al. 2018b; Jiménez-Donaire et al. 2019). The reason for this is that we are resolving structures within this region, such as the nuclear region (NUC; inner −0.15 kpc) that appears to exhibit SFE$_{\text{dense}}$ enhancements relative to the rest of the centre.

We test line ratio diagnostic plots and compare our high-resolution (150 pc) dense gas tracer towards NGC 6946 with those of eight other galaxy centres in the EMPIRE survey (angular resolution of 33′′ ∼ 1 kpc) and discuss implications for other galaxy centre studies.

7) From previous studies higher CO (1−0) to CO (2−1) ($R_{21}$) values are expected in the inner kiloparsec compared to their disc. We find $R_{21}$ variations in the centre; higher $R_{21}$ in NBE (−0.7) than in the NUC or SBE (−0.65 and −0.62). The reason for this could be, for example, denser gas that is in the NBE. However, we do not find an increase of higher $f_{\text{dense}}$ in NBE (see Fig. 7 and Table 7).

8) Whether the ratio between HCN and HNC is temperature dependent has been discussed by several authors in the past. We speculate that the isomer ratio is not an accurate probe for kinetic temperatures for kiloparsec and sub-kiloparsec sized extragalactic regions. This is because, if the prescription of Hacar et al. (2020) can be applied here, the HCN/HNC ratio results in low $T_{K}$ (<50 K, for NGC 6946 as well as for six EMPIRE galaxies, IC 342 and NGC 253) which is up to a factor of 7 lower compared to other existing $T_{K}$ measurements (NH$_{3}$ or H$_{2}$CO).

9) The observed HCO$^{+}$/HNC ratios have been proposed to be a diagnostic tool to distinguish between XDR and PDR. The diagnostic plots for the centre of NGC 6946 favour a PDR. We find that an X-ray source about 2′′ away from the dynamical centre does not affect the molecular gas properties in the nucleus. However, when we include the EMPIRE galaxy centres in our analysis, we find that those galaxies that have an active galactic nucleus (AGN) fall within the PDR range in these diagnostic diagrams. We find for two of these AGN host galaxies higher resolution observations (∼100pc for NGC 3627 and ∼166pc for M51) which also lay in the PDR regime. Thus, the HCO$^{+}$/HNC ratio might not be a unique indicator to diagnose AGN activity in galaxies at (sub-)kiloparsec scales. This ambiguity is consistent with recent studies (see Fig. 8 and Section 6.3).
10) Molecular line ratios may reflect changes in the (unresolved) gas density distributions (Leroy et al. 2017). The ratios to CO, show enhanced line ratios within the NUC compared to the SBE. We quote the mean values over each region that are equivalent to our beam size of 4″ ≈ 150 pc.

| Unit                  | NUC       | NBE       | SBE       | Notes |
|-----------------------|-----------|-----------|-----------|-------|
| $I_{\text{CO}(2-1)}$ | 587.3±1.51| 388.6±0.86| 438.5±1.68| 3     |
| $I_{\text{HCN}}$     | 67.9±0.39 | 35.19±0.37| 40.12±0.36| 3     |
| $I_{\text{CH}_3\text{OH}}$ | 7.15±0.45 | 5.17±0.40 | 11.53±0.35| (1)   |
| $SFR$                 | 2.43±0.24 | 2.98±0.34 | 8.85±0.50 | (1)   |
| $SFR_{\text{HCO}^+}/I_{\text{CO}}$ | 433      |            | 872       |       |

Notes: We quote the mean values over each region that are equivalent to our beam size of 4″ ≈ 150 pc. NUC = Nuclear Region; NBE = northern inner bar end; SBE = southern inner bar end.

(1): Taken from our extended molecular data set – PdBI only. CH$_3$OH is the (2k-1) transition and CO the (2-1) transition.

(2): In units of K km s$^{-1}$/(M$\odot$ yr$^{-1}$ kpc$^{-2}$)

(3): If the Hacar et al. (2020) framework holds valid in NGC 6946; see detailed discussion in Section 6.2.

This study reflects the importance of analysing molecular lines to better understand galactic centres. Also, it shows that bar ends in galaxies can vary in their dense gas fraction, star formation rate, integrated line ratios and molecular gas densities. In future work we follow up on the investigation of shocks, the densest gas tracers in our extended data set and examine the kinematic and dynamic of the inner bar in more detail.

Acknowledgements. We would like to thank the anonymous referee for their insightful comments that helped improve the quality of the paper. CE gratefully acknowledges funding from the Deutsche Forschungsgemeinschaft (DFG) Sachbeihilfe, grant number BI1546/5-1. FB, AB, IB, JP and JD acknowledge funding from the European Research Council (ERC) under the European Union’s Horizon 2020 research and innovation programme (grant agreement No.726384/Empire). ES, DL, HAP, TS and TGW acknowledge funding from the European Research Council (ERC) under the European Union’s Horizon 2020 research and innovation programme (grant agreement No. 694343). IL acknowledges funding from the Deutsche Forschungsgemeinschaft (DFG) Sachbeihilfe, grant number SCHR 536/11-1. MC and JD acknowledge support of the Natural Sciences and Engineering Research Council of Canada (NSERC), funding reference RGPIN-2017-03987. AKL acknowledges support from the National Science Foundation under Grants No. 1615105, 1615109, and 1653300. JP acknowledges support from the Programme National “Physique et Chime du Milieu Interstellaire” (PCMI) of CNRS/INSU with INC/INP co-funded by CEA and CNES. MQ acknowledges support from the Spanish grant PID2019-106027GA-C44, funded by MCIN/AEI/10.13039/50110001033 and by “ERDF A way of making Europe”, and PID2019-108765GB-I00, funded by MCIN/AEI/10.13039/50110001033. Y-HT acknowledges funding support from NRAO Student Observing Support Grant SOSPADA-012 and from the National Science Foundation (NSF) under grant No. 2108081.

References

Aalto, S., Polatidis, A. G., Hüttemeister, S., & Curran, S. J. 2002, A&A, 381, 783
Aladro, R., Viti, S., Bayet, E., et al. 2013, A&A, 549, A39
Aalto, S., Rizzo, L., & Tully, R. B. 2018, AJ, 156, 105
Ao, Y., Henkel, C., Menten, K. M., et al. 2013, A&A, 550, A135
Astropy Collaboration, Price-Whelan, A. M., Sipőcz, B. M., et al. 2018, AJ, 156, 123
Astropy Collaboration, Robitaille, T. P., Tollerud, E. J., et al. 2013, A&A, 558, L3
Baan, W. A., Henkel, C., Loenen, A. F., Baudry, A., & Wilkinds, T. 2008, A&A, 477, 747
Barnes, A. T., Kruehler, J., Bigiel, F., et al. 2020a, MNRAS, 497, 1972
Barnes, A. T., Longmore, S. N., Aravena, A., et al. 2019, MNRAS, 486, 283
Barnes, A. T., Longmore, S. N., Battersby, C., et al. 2017, MNRAS, 469, 2263
Barnes, A. T., Longmore, S. N., Dale, J. E., et al. 2020b, MNRAS, 498, 4006

Table 7. Summary of the characteristics of the nuclear region and inner bar ends of NGC 6946 based on the analyses in this work.

| Unit                                      | NUC       | NBE       | SBE       | Notes |
|-------------------------------------------|-----------|-----------|-----------|-------|
| $I_{\text{CO}(3-1)}$                      | 842.75±2.43| 565.91±2.23| 705.35±2.25| 3     |
| $I_{\text{HCN}}$                          | 587.3±1.51| 388.6±0.86| 438.5±1.68| 3     |
| $I_{\text{HCN}}$                          | 67.9±0.39 | 35.19±0.37| 40.12±0.36| 3     |
| $I_{\text{CH}_3\text{OH}}$                | 7.15±0.45 | 5.17±0.40 | 11.53±0.35| (1)   |
| $SFR$                                     | 2.43±0.24 | 2.98±0.34 | 8.85±0.50 | (1)   |
| $SFR_{\text{HCO}^+}/I_{\text{CO}}$        | 433       |            | 872       |       |
Appendix A: Star formation rates

In this work, we used the 33 GHz continuum emission as a SFR tracer. We also found published 15 GHz and Hα observations in comparable angular resolution of our molecular data set (2′′; see Table A.1). We chose the 33 GHz over the 15 GHz as a SFR tracer because the 33 GHz observations are: (1) higher in sensitivity (9.72 compared to 21.44 mK, Linden et al. 2020), and (2) probe less non-thermal emission (38% compared to 63%, see Equations below). We did not use extinction corrected Hα data (from Kessler et al. 2020) for our main SFR in this paper because: (1) they used 2′′ sized apertures across the whole galaxy covering the bright Hα emitting regions (1σ threshold in Hα) for the extinction correction (using Paβ) and those apertures do not fully cover the inner kpc of NGC 6946, and (2) causes them to miss a handful of heavily attenuated regions in the centre of NGC 6946 (see Fig. 2 in Kessler et al. 2020).

In the following we check the consistency of our SFR derived from the 33 GHz thermal part of the radio continuum emission with the thermal part of the 15 GHz as a SFR tracer (observations from Murphy et al. 2018 and Linden et al. 2020) for the inner kpc-sized region of NGC 6946.

1. 33 GHz continuum: Using 33 GHz for the inner 1 kpc gives us a mean \(\Sigma_{\text{SFR}}\) of 0.792 M\(_{\odot}\) yr\(^{-1}\) kpc\(^{-2}\).

2. 15 GHz continuum: Before we can use Eq. (4), we first have to compute the thermal fraction \(f^T\) at 15 GHz. We recall that we denote thermal as \(T\), non-thermal as \(NT\) and the frequency as \(\nu\). Knowing that \(S_T^\nu \propto \nu^{-\alpha_T}\) with \(\alpha_T \sim 0.1\) and \(S_{NT}^\nu \propto \nu^{-\alpha_{NT}}\) with \(\alpha_{NT} \sim 0.74\) (from Murphy et al. 2011 for the nucleus of NGC 6946), we find:

\[
f^{T}_{15\text{GHz}} = \left( \frac{f^{T}_{33\text{GHz}}}{S^{T}_{33\text{GHz}} / S^{NT}_{33\text{GHz}}} \right) \times \left( \frac{S^{T}_{15\text{GHz}} / S^{NT}_{15\text{GHz}}}{} \right).
\]  

(A.1)

We take as in Section 2.3.2 \(f^{T}_{33\text{GHz}} = 0.62\) and find using Eq. (A.1) that \(f^{T}_{15\text{GHz}} = 0.37\). Now we are able to calculate \(L_T\) (Eq. (5)) and use Eq. (4) to convert the thermal fluxes into a SFR and further to \(\Sigma_{\text{SFR}}\). Within the central kpc-sized region we get a mean \(\Sigma_{\text{SFR}}\) of 0.774 M\(_{\odot}\) yr\(^{-1}\) kpc\(^{-2}\).

We conclude, that the \(\Sigma_{\text{SFR}}\) for the inner kpc derived from 33 GHz and 15 GHz are within the margin of error (~1σ).

Appendix A.1: Correcting for distance

Schinnerer et al. (2007) found within a 3′′ × 3′′ region a SFR of ~0.1 M\(_{\odot}\) yr\(^{-1}\) adopting a distance of 5.5 Mpc. Using 33 GHz as a SFR tracer and taking the same distance and region, we get 0.06 M\(_{\odot}\) yr\(^{-1}\). Adopting the updated distance to NGC 6946 of 7.72 Mpc results in 0.11 M\(_{\odot}\) yr\(^{-1}\). This is only a factor of 1.8 higher.
Table A.1. References of the data shown in Fig 1.

| Panel in Fig 1 | λ, L | Instrument | Res. | Survey, Reference |
|----------------|------|------------|------|-------------------|
| (a, b)          | 200  | optical    |      | HST, Subaru       |
|                 | 300  |            |      | NASA, ESA, STScI, R. Gendler and the Subaru Telescope (NAOJ) |
| (c)             | 115  | GHz        | 1.4''| Schinnerer et al. (2006) |
| (d)             | 230  | GHz        | 0.4''| Schinnerer et al. (2006) |
| (e)             | 3    | GHz        | 2.0''| Schinnerer et al. (2006) |
| (f)             | 15   | GHz        | 2.1''| Schinnerer et al. (2006) |
| (g)             | 33   | GHz        | 2.1''| Schinnerer et al. (2006) |
| (h)             | 70   | µm         | 5.5''| KINGFISH, Kennicutt et al. (2011) |
| (i)             | 24   | µm         | 5.7''| SINGS, Kennicutt et al. (2003) |
| (j)             | 8    | µm         | 2.0''| SINGS, Kennicutt et al. (2003) |
| (k)             | Paβ  |            |      | KESSLER et al. (2020) |
| (l)             | Hα   | 3.5-m      | 2.0''| Long et al. (2019); Kessler et al. (2020) |
| (m)             | X-ray|            |      | ObsIDs 1054 and 13435, Holt et al. (2003) |

Notes: To overlay the contours of CO data on the optical images, we used [http://nova.astrometry.net/](http://nova.astrometry.net/)

Fig. A.1. SSC + uv trim integrated intensity maps: The way of presenting the data is done as in Figure 2. Here, however, we performed a $u-v$ cut and corrected for the short-spacing using available EMPIRE data for the three typical dense gas tracers. In the first two panels we show contours of 200, 300$\sigma$ and in the remaining three panels contours of 3, 6, 9, 30, 60, 90$\sigma$. 
Fig. A.2. Same as Figure 2 but only showing hexagonal points with $S/N > 25$ for CO (1−0) and CO (2−1), and with $S/N > 5$ for all other lines.
Fig. A.3. HCN channel maps, from $-80$ to $110$ km s$^{-1}$.
Fig. A.4. HCO$^+$ channel maps, from $-80$ to $110$ km s$^{-1}$. 
Fig. A.5. HNC channel maps, from -80 to 110 km s$^{-1}$. 
Fig. A.6. CS(2-1) channel maps, from -80 to 110 km s$^{-1}$.
**Fig. A.7.** CS(3-2) channel maps, from -80 to 110 km s$^{-1}$. 
Fig. A.8. N$_2$H$^+$ channel maps, from -80 to 110 km s$^{-1}$. 
Fig. A.9. CH$_3$OH(2k-1k) channel maps, from -80 to 110 km s$^{-1}$. 
Fig. A.10. CH$_3$OH(3k-2k) channel maps, from -80 to 110 km s$^{-1}$. 
Fig. A.11. $\text{C}_2\text{H}(1-0)$ channel maps, from -80 to 110 km s$^{-1}$. 
Fig. A.12. HC$_3$N(10-9) channel maps, from -80 to 110 km s$^{-1}$. 
Fig. A.13. HC$_3$N(16-15) channel maps, from -80 to 110 km s$^{-1}$.
Fig. A.14. $\text{H}_2\text{CO}(2-1)$ channel maps, from -80 to 110 km s$^{-1}$. 