NON-LTE INVERSIONS OF THE Mg II h & k AND UV TRIPLET LINES

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ABSTRACT

The Mg II h & k lines are powerful diagnostics for studying the solar chromosphere. They have become particularly popular with the launch of the Interface Region Imaging Spectrograph (IRIS) satellite, and a number of studies that include these lines have lead to great progress in understanding chromospheric heating, in many cases thanks to the support from 3D MHD simulations. In this study, we utilize another approach to analyze observations: non-LTE inversions of the Mg II h & k and UV triplet lines including the effects of partial redistribution. Our inversion code attempts to construct a model atmosphere that is compatible with the observed spectra. We have assessed the capabilities and limitations of the inversions using the FALC atmosphere and a snapshot from a 3D radiation-MHD simulation. We find that Mg II h & k allow reconstructing a model atmosphere from the middle photosphere to the transition region. We have also explored the capabilities of a multi-line/multi-atom setup, including the Mg II h & k, the Ca II 854.2 nm, and the Fe I 630.25 lines to recover the full stratification of physical parameters, including the magnetic field vector, from the photosphere to the chromosphere. Finally, we present the first inversions of observed IRIS spectra from quiet-Sun, plage, and sunspot, with very promising results.

Key words: Sun: atmosphere – Sun: chromosphere – polarization – radiative transfer

1. INTRODUCTION

The solar chromosphere forms the interface region between the solar interior and the hot corona. Understanding the chromosphere is of great interest to solar and stellar physics because the energy that heats the corona, the mass lost in the solar wind, and the magnetic flux that forms the coronal magnetic field pass through it. It is difficult, though, to derive the physical state and evolution of the chromosphere because it shows complex spatial and temporal restructuring down to scales that cannot be resolved with current instruments. In addition, the UV and optical continua and lines that make up the bulk of the diagnostics form under optically thick non-LTE conditions so that a straightforward interpretation of the observed spectra is not possible. A promising avenue into systematically interpreting spatially resolved chromospheric observations are non-LTE inversions. Such inversions create a best-fit atmospheric model that is consistent with the observations (e.g., Socas-Navarro et al. 2000, 2015).

The Interface Region Imaging Spectrograph (IRIS; De Pontieu et al. 2014) has provided a new spatially and temporally resolved view of the upper chromosphere. The richest IRIS diagnostics are the Mg II h & k and Mg II UV triplet lines (Leenaarts et al. 2013; Pereira et al. 2015). We present a new inversion code that can take into account non-LTE lines and continua including the effects of partial redistribution (PRD) for multiple atoms simultaneously. We apply the code to synthetic spectra as well as IRIS observations. The broad wings of the Mg II h & k lines and the finite spectral window observed with IRIS lead to a limited sensitivity of the lines to photospheric conditions. In addition, the calculations by, e.g., Goldberg (1957) and Carlsson et al. (2015) indicate a level of degeneracy in the response of the intensity profile with respect to variations in temperature and microturbulence. We therefore also investigate whether multi-line, multi-atom inversions using a combination of the Mg II h & k, Mg II UV triplet, Ca II 854.2 nm, and Fe I 630.2 nm yield improved inference of the atmosphere, among others that could also be used.

2. METHOD

We have incorporated a non-LTE radiative transfer engine based on the RH code (Uitenbroek 2001) to a newly developed inversion framework including some of the ideas presented in Asensio Ramos & de la Cruz Rodríguez (2015).

RH has become the workhorse non-LTE radiative transfer code in solar physics owing to its flexible nature and comprehensive inclusion of the relevant physics. An important aspect of RH is that it includes the effect of PRD, including a fast approximation of angle-dependent PRD (Leenaarts et al. 2012) that allows for fast computation of accurate Mg II h & k line profiles in models with varying vertical velocity. In our inversion code, we run RH to solve the non-LTE radiative transfer problem for a given stratification of temperature, hydrogen populations, electron density, vertical velocity, and microturbulence as a function of optical depth. Response functions (RFs) are computed numerically. The model atmosphere is initialized by specifying the temperature, velocity, and microturbulence for a given optical-depth scale. The hydrogen density, electron density, and height scale are then computed using an LTE equation of state (Piskunov & Valenti 2016) and hydrostatic equilibrium. The inversions can be performed in full-Stokes mode or intensity-only mode. When mixing spectral region with and without polarization, the code runs in full-Stokes mode and the unpolarized regions are given zero weight in Stokes Q, U, and V.

The physical quantities of the model are discretized using a small number of node points (Ruiz Cobo & del Toro Iniesta 1992). To produce a fully depth-stratified atmosphere, the nodes are connected using a second-order piece-wise Bezier-spline (de la Cruz Rodríguez & Piskunov 2013). The depth resolution is given by the number and location of the nodes that are used for each physical parameter.
We assume plane-parallel geometry and statistical equilibrium to calculate the atomic level populations in each pixel (1.5D), a necessary compromise to make the inversion problem treatable. We compute the RF based on the wavelength grid and instrumental spectral smearing of the near-UV window of the IRIS spectrograph (δλ = 2.54 pm). To speed up the calculations, we have used a coarser sampling of 20.36 pm in the extended wings of the Mg II h & k lines, but we kept the full sampling close to the line cores. This reduced the number of wavelengths by a factor of three. The result of the inversion is insensitive to very fine sampling in the broad and slow-varying wings of Mg II h & k.

For the multi-line, multi-atom inversions we include a frequency grid based on critically sampled line profiles with the CRISP instrument on the Swedish 1 m Solar telescope (Scharmer et al. 2003; Scharmer et al. 2008).

In Sections 3.1 and 3.2, we have computed synthetic observations with RH working in full-Stokes mode and assuming 1.5D radiative transfer. We used the same fast PRD approximation that is used during the inversions. In the first cycle, we used four nodes in temperature, three nodes in vertical velocity and microturbulence, magnetic field strength, azimuth, and inclination. The second cycle was initialized from the atmosphere inferred in the first cycle using seven nodes in temperature; three nodes in vertical velocity and microturbulence, magnetic field strength, and inclination; and one node in azimuth. We have given zero weight to Stokes Q, U, and V in the Mg II spectral window to simulate an IRIS observation.

Figure 1 shows the results. The inversions succeed in matching the synthetic observations precisely. The temperature is matched well for \(\log_{10} \tau_{500} < -5\), and the inversions are worse since the radiation is only weakly coupled to the local conditions of the model at those heights. Nevertheless, the code manages to mimic the shape of the transition region relatively well. According to this test, the Mg II lines alone (light blue) can constrain the temperature stratification.

3. RESULTS

3.1. Inversions of the FALC Model

As a first test we inverted line profiles from the FALC 1D semi-empirical model atmosphere of Fontenla et al. (1993). We changed the microturbulence from the original form to a smoother slightly convex profile in \(\log_{10} \tau_{500}\), added a magnetic field with gradients in strength and inclination and a constant azimuth, and added a linear gradient in vertical velocity as a function of optical depth. The inversions were performed in two cycles, improving the convergence and speed of the inversion (Pietarila et al. 2007). In the first cycle, we used four nodes in temperature, three nodes in vertical velocity, two nodes in microturbulence, and one node in magnetic field strength, azimuth, and inclination.

The second cycle was initialized from the atmosphere inferred in the first cycle using seven nodes in temperature; three nodes in vertical velocity and microturbulence, magnetic field strength, and inclination; and one node in azimuth. We have given zero weight to Stokes Q, U, and V in the Mg II spectral window to simulate an IRIS observation.

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reasonably well. The reconstruction of the deeper photosphere improves when the Ca II 854.2 nm line is included (orange red), and it is almost perfect when we include the Fe I line (navy blue). The vertical velocity and microturbulence stratifications are retrieved by the inversion scheme relatively well at all depths, but adding the Fe I and the Ca II lines improves the estimate of the vertical velocity in the deepest layers of the atmosphere. These results are somewhat expected because the broad wings of the Mg II lines are sensitive to the temperature stratification, but the small intensity gradient makes the wings insensitive to changes in the vertical velocity at \( \log t_{7500} > -3 \).

The Ca II line constrains the magnetic field strength between \(-6 < \log t_{7500} < -4\), but the shape of the gradients are not reproduced very well. Only when the Fe I line is included are the entire field strength profiles properly retrieved for this configuration of the magnetic field. The magnetic field inclination is reconstructed accurately in both cases for the assumed noise levels. All combined, these lines appear to be a powerful tool to retrieve the full depth-stratification of the solar atmosphere, including the magnetic field vector.

This test also shows that even in a quiet-Sun model as FALC there is enough coupling to the local physical conditions present in the input model for the inversion to work. The FALC test model atmosphere is very smooth, so in Section 3.2 we test inversions of a 3D MHD simulation containing strong gradients.

### 3.2. Inversions of a Radiation-MHD Model

In this section, we present a setup that can be used to invert IRIS Mg II data alone, as co-observations with other facilities are not always available.

We have calculated synthetic profiles from a vertical slice through from the publicly available 3D MHD simulation of enhanced network that was performed with the Bifrost code (Gudiksen et al. 2011; Carlsson et al. 2016). This slice cuts through two patches of magnetic bright points and through the fibril-like features that are formed between them, extending from pixel \((x, y) = (69,206)\) to \((x, y) = (431,339)\). This simulation includes the effects of non-equilibrium hydrogen ionization that has an effect on the electron density in the chromosphere and transition region (Leenaarts et al. 2007) and unlike FALC, it is not in hydrostatic equilibrium. We have degraded the synthetic profiles to the spectral resolution of IRIS and have added Gaussian noise with standard deviation \(\sigma = 2 \times 10^{-3}\). We have estimated a similar noise level from the wings of the Mg II lines in IRIS observations.

Our experiment with the FALC model provides evidence that velocities in the photosphere are poorly constrained when the Mg II lines are used exclusively. We have also included the Ni I 281.4350 nm line to better constrain velocities in the photosphere. This is one of the weakest, relatively unblended, lines in the same IRIS spectral window as Mg II h & k. Because the line is weak, we can include it in the inversion assuming LTE. We suspect there are more similar lines that could in principle also be included.

We ran the inversions in two cycles as described in Section 3.1, ending with seven nodes in temperature and four nodes in vertical velocity. Our results are presented in Figure 2. The top row displays the temperature and vertical velocity on the original height scale of the simulation. The second row shows these properties on a per-pixel \( \log t_{7500} \) scale. The third row displays how the slices look if we represent them using seven nodes in temperature and four nodes in vertical velocity connected by Bezier-splines. This illustrates the kind of depth resolution that we can expect from the inversions. Finally, the inversion results are shown in the last row.

**Temperature.** The inverted temperatures shown in panel (d) resemble those in panel (b), given the limitations of the node representation. In fact, there are regions that resemble the original atmosphere better than those in the interpolated model in panel (c), probably because the inversion can adjust the values of the nodes to fit the gradient of the spline that is connecting them, whereas the plain interpolation in panel (c) is very sensitive to the local value of the atmosphere at the locations of the nodes. Close to the transition region, around \( \log t_{7500} = -6 \), there are atmospheric features that are well reconstructed in the majority of the columns, but the overall transition region temperature increase appears at larger optical depth in the inversion.

**Line of sight velocity.** The reconstructed line of sight velocities are shown in panel (h) of Figure 2. In comparison with the original bifrost slice in panel (f), the resemblance is a bit worse than in the temperature case. We have experimented with the number of nodes used in this parameter with similar results: velocities in the very upper layers of the model typically have the same sign as the original slice but have larger amplitudes.

Figure 3 shows in detail the results from the inversion of two Bifrost columns \((x = 9.6\) and \(x = 15.6\) Mm). These plots illustrate that our code can reproduce the large scales present in the input model atmosphere, but not the small-scale features. The node-based parameterization is not able to reproduce sharp plato-like areas in the upper chromosphere, like the one in the left column around \( \log t_{7500} = -6 \). This is probably one of the reasons why we get a hotter transition region in some columns. However, the effect of not including non-equilibrium hydrogen ionization can also be partly responsible in some areas. Our EOS assumes LTE ionization and the inversion can compensate the lower-LTE electron density by increasing the temperature close to the transition region.

### 3.3. Inversions of IRIS Data

We applied our inversion code with an IRIS observation of active region NOAA AR 12104 acquired on 2014 July 4 at 11:40 UT. The data set consists of a 400 step raster with an exposure time of 30 s per slit position and 5.3 pm spectral resolution. This observation was previously used by Carlsson et al. (2015).

We inverted three spectra formed in quiet-Sun (gray-cross), plage (blue-cross), and quiescent sunspot (orange-cross) regions. The field of view and the location of the pixels are shown in Figure 4. The images in the top row depict monochromatic images in the blue wing of the k line, in the core of one of the subordinate triplet lines and in the core of Mg II k.

We included the photospheric Ni I line that we used in the previous experiment. The inversions were again performed in two cycles, ending with seven nodes in temperature and four nodes in vertical velocity and three nodes in microturbulence to invert the plage and quiet-Sun profiles. The sunspot profile was inverted using one node in velocity (see the discussion below). We initialized the inversions with a smoothed version of FALC with a constant microturbulence
We chose the umbra of the sunspot during quiescence as a rough zero velocity reference. Our results are shown at the bottom of Figure 4. The code fits all three cases quite well. The best fit to the quiet-Sun profile is very good except for small discrepancies in the core of some of the lines. The resulting model has a cooler chromosphere and transition region than FALC, which is somewhat expected given that the \( h_2 \) and \( k_2 \) intensities are lower than those predicted from FALC. The inversion code has reconstructed a velocity gradient needed to reproduce the location and the asymmetries close to line center. The LOS velocity in the photosphere is mostly constrained by the Ni I line. The microturbulence profile starts at zero in the photosphere and it increases almost linearly to 3 km s\(^{-1} \) in the upper chromosphere, which is similar to the average chromospheric value of the FALC model.

We have fitted the quiescent sunspot profile with a single node in velocity. Adding more nodes did not improve the best fit, and we found out that including more nodes could also lead to a solution where the central line depressions are suppressed by introducing a very step gradient in velocity, instead of filling up the core with adjustments in the temperature profile. The observed profile is also very well fitted, except for the innermost line positions in the \( h \) & \( k \) lines. Further experiments with the number of nodes showed that the inner core is sensitive to the exact location of the transition region. The reconstructed temperature profile reaches a minimum at \( \log_{10} \tau_{7500} = -2.5 \), and it smoothly increases toward the chromosphere. The transition region is located at higher optical depth than in the quiet-Sun example. The code sets the microturbulence to almost zero, except for the very upper layers where it increases again.

The plage profile is qualitatively well reproduced by our best fit. We have increased the gas pressure at the upper boundary of the model atmosphere by more than one order of magnitude (like Shine & Linsky 1974), which is used to start the hydrostatic equilibrium integration. Otherwise, we could not get sufficient emission in the line cores even for very high temperatures. The temperature stratification that we derive is surprisingly similar to the model presented in Carlsson et al.

Figure 2. Vertical slice through the simulation snapshot. Left-hand panels: temperature. Right-hand panels: line of sight velocity. Top to bottom: the original model, the original model on a regular \( \log_{10} \tau_{7500} \) depth scale, the original model degraded to a representation using seven nodes, and the results from the inversions.
of the transition region sets strong constraints on the inversion of temperatures and sometimes velocities.

4. DISCUSSION AND CONCLUSIONS

We have included the effect of PRD in a non-LTE inversion code to study the Mg II h & k lines. We have performed tests with the FALC model atmosphere and with a 3D MHD simulation to show that the inversion code is able to retrieve information in the upper layers of the solar chromosphere. Throughout this study we have assumed that we can model the Mg II h & k lines using plane-parallel radiative transfer, which can be a serious approximation in the core of strong lines. The 1.5D approximation used in our inversions usually leads to higher contrast in the emerging intensity maps when compared to a full 3D evaluation because horizontal radiative transfer has a smoothing effect. The inversion code normally compensates for 3D effects by decreasing the contrast in the retrieved temperature maps (de la Cruz Rodríguez et al. 2012). The results of Sukhorukov & Leenaarts (2016) indicate that the plane-parallel approximation is reasonable for inversions with the Mg II h & k lines at disk center, but one should keep in mind that this approximation is a varying source of errors that depend on the structure of the atmosphere surrounding our pixel. Especially close to large horizontal gradients in the atmosphere the errors may be large.

Our results with the radiation-MHD model are particularly encouraging because this model includes the effects of non-equilibrium hydrogen ionization and is not in hydrostatic equilibrium, yet the inversions can in most cases retrieve a similar temperature stratification to that in the input model atmosphere and provide good estimates of line of sight velocities even when only the Mg II h & k and UV lines are
included. The addition of more diagnostics, especially those sensitive to different regimes and temperatures in the atmosphere, should help to further constrain the quality of the reconstruction.

We have presented the first inversions of spatially resolved IRIS spectra from typical quiet-Sun, plage, and sunspot profiles. Our plage inversions require very high values of microturbulence in the upper photosphere to reproduce the width of the

Figure 4. Top row: monochromatic images illustrating the location of our selected pixels for the inversion taken in the blue wing of the k line, in the core of the UV line, and in the core the k line. Left column: observed spectra (black) and best-fit (red) for quiet-Sun, sunspot, and plage pixels, respectively, from top to bottom. The inset depicts a zoom in the core of Mg II k. The reconstructed temperature (black), $v_{\text{LOS}}$ (red), and $v_{\text{turb}}$ (blue) stratifications are shown in the right column.
profile, which in itself is very interesting because it points to a physically different situation compared to quiet Sun and sunspots. Unfortunately, we still do not understand the nature of this enhanced microturbulence. We believe that the addition of more non-LTE diagnostics from other atomic species can help to understand it. The Ca II H & K lines and the Ca II IR triplet lines are very good candidates for such an addition.

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