Synthetic phonons enable nonreciprocal coupling to arbitrary resonator networks

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Inducing nonreciprocal wave propagation is a fundamental challenge across a wide range of physical systems in electromagnetics, optics, and acoustics. Recent efforts to create nonreciprocal devices have departed from established magneto-optic methods and instead exploited momentum-based techniques such as coherent spatiotemporal modulation of resonators and waveguides. However, to date, the nonreciprocal frequency responses that these devices can achieve have been limited, mainly to either broadband or Lorentzian-shaped transfer functions. We show that nonreciprocal coupling between waveguides and resonator networks enables the creation of devices with customizable nonreciprocal frequency responses. We create nonreciprocal coupling through the action of synthetic phonons, which emulate propagating phonons and can scatter light between guided and resonant modes that differ in both frequency and momentum. We implement nonreciprocal coupling in microstrip circuits and experimentally demonstrate both elementary nonreciprocal functions such as isolation and gyration, as well as reconfigurable, higher-order nonreciprocal filters. Our results suggest nonreciprocal coupling as a platform for a broad class of customizable nonreciprocal systems, adaptable to all wave phenomena.

INTRODUCTION

The interactions between elementary particles and quasi-particles (electrons, photons, and phonons) are dictated by both momentum and energy conservation; this is broadly termed as phase matching. These conservation laws are especially important in the field of nonlinear optics (1), as inelastic scattering of light involving the creation or annihilation of propagating phonons can produce large shifts in photon momentum (2–4). Phonon-assisted momentum shifts in turn permit unique phenomena such as indirect interband photonic transitions (5–9), where light is scattered between optical modes that differ in both frequency and momentum. Indirect interband transitions and similar processes associated with significant momentum shifts have recently been identified as promising tools for inducing nonreciprocal transmission of light (5, 6, 10–22) and sound (23, 24) without reliance on magnetic fields. Devices based on these effects break Lorentz reciprocity because momentum shifts are not symmetric under time reversal (25), for example, if an incoming wave scatters and gains momentum, then a time-reversed copy of the wave will lose momentum in the same process.

To date, nonreciprocal devices based on indirect photonic transitions have exclusively relied on scattering between copropagating modes in waveguides (6, 11, 13, 14) or resonators (17, 18, 21). Here, we demonstrate that indirect transitions can also be induced between a guided mode and a stationary resonant mode (Fig. 1A) through the action of synthetic phonons, which emulate propagating phonons but have independently controlled frequency and momentum. These indirect transitions effectively generate nonreciprocal coupling between the guided and resonant modes, as only one propagation direction is coupled to the resonance. As we will show, the power of nonreciprocal coupling is that highly tailorable, reconfigurable nonreciprocal transfer functions can be arranged using conventional waveguides and resonators.

It is important to note a major difference between indirect transitions among copropagating modes and nonreciprocal coupling between a guided and a resonant mode. In a closed (lossless) system, the copropagating modes of a waveguide or resonator are orthogonal. These modes are not coupled unless a bias is applied that breaks their orthogonality. By contrast, resonant modes often couple to guided modes. This coupling is reciprocal, making it undesirable in systems using nonreciprocal coupling. To ensure that only nonreciprocal coupling occurs in our system, we intentionally create a phase mismatch between the guided and resonant modes. Throughout this paper, we refer to such phase mismatched resonant modes as dark states because, analogous to atomic dark states (26, 27), they are localized resonances that cannot emit or absorb light. These dark states are an example of parametric bound states in the continuum (28). Dark states have previously been studied for applications in photonics (29–31) and have several properties, namely suppressed emission and long lifetime, that are especially useful for creating nonreciprocal devices.

We begin our discussion with a generalized system consisting of a waveguide and resonator that are coupled at multiple spatially separated coupling sites, as shown in Fig. 1B. We first describe how the interference between these coupling sites can be exploited to suppress interactions between the waveguide and resonator and create a dark state. We then show that time modulation of the coupling constant at each site emulates the effect of driven phonons and can re-enable interactions between the prepared dark state with only one propagation direction within the waveguide (Fig. 1A). When photons arrive from the right, their frequency and momentum are both decreased by the phonon-biased coupling, and the photons can enter the dark state. By contrast, when photons arrive from the left, the same frequency and momentum shifts result in an overall increase in photon momentum such that the photons cannot enter the dark state. This asymmetry in the total photon momentum is the fundamental principle behind nonreciprocal coupling.

The form of our proposed coupling rate modulation, which we term as a “synthetic phonon,” is depicted in Fig. 1B. Synthetic phonons are analogous to phonons in a crystal lattice: Coupling sites are equivalent to lattice sites, and the varying coupling rate is equivalent to atomic displacement. In contrast to phonons in a crystal, the synthetic phonon momentum is externally controlled and does not depend on an intrinsic dispersion relation, allowing synthetic phonons to be applied in a wide variety of situations without the added complexity of dispersion engineering (14). We experimentally realize synthetic phonons in microwave
frequency microstrip circuits by sinusoidally modulating the capacitive coupling rate of spatially separated variable capacitors. Using these synthetic phonons, we experimentally demonstrate several distinct nonreciprocal effects including extreme isolation contrast (>82 dB), nonreciprocal phase shifts, and higher-order nonreciprocal filters.

RESULTS

Nonreciprocal coupling to engineered dark states

We consider our representative system (Fig. 1B) consisting of a two-port waveguide having a frequency-dependent propagation constant $k$ and a resonator supporting a single mode at angular frequency $\omega_0$. The resonator is side-coupled to the waveguide at $N$ independent sites that are evenly separated on the waveguide by a constant length $\ell$. For simplicity, we assume that each coupling site is located at the same spatial location on the resonator and that the waveguide is lossless and only supports a single mode. We define forward propagation in the waveguide from port 1 toward port 2.

This system can be characterized by analyzing the coupling between the waveguide and the resonator using the framework of temporal coupled-mode theory (32, 33). Since each coupling site is independent, the coupling constants $C_1$ and $C_2$ between the waveguide and resonator (see Fig. 1C) are evaluated as a superposition of the contributions from each site

$$C_1 = \sum_{n=1}^{N} c_n e^{-ik(n-1)}, C_2 = \sum_{n=1}^{N} c_n e^{ik(n-1)}$$

where $c_n$ is the coupling constant at the $n$th site. The exponential term in these definitions accounts for propagation in the waveguide between adjacent coupling sites spaced by $\ell$ and differs between $C_1$ and $C_2$ due to the opposite propagation directions. The coupling constants are also related to the resonator’s decay, which can be described by the decay rate $\gamma = (\kappa_i + \kappa_{ex})/2$. Here, $\kappa_i$ is the intrinsic decay rate of the resonator, and $\kappa_{ex} = |C_1|^2 + |C_2|^2$ is the external decay rate due to coupling with the waveguide (33).

Equation 1 reveals that the contribution from the $n$th coupling site carries a phase $k\ell(n-1)$. When summed, these contributions interfere such that the maximum coupling rate occurs only if all $N$ contributions are in-phase (phase-matched coupling). The coupling rate decreases away from this maximum and reaches zero when the contributions perfectly destructively interfere. In the case of a complete phase mismatch, we obtain $\kappa_{ex} = 0$, and the resonator can be classified...
as a dark state since it cannot be excited by (or decay to) the waveguide. Since phase matching in this system is determined by the product $k\ell$, it is possible to arrange a dark state from an arbitrary waveguide and resonator by selecting the appropriate \( \ell \).

We now discuss how a dark state created by a total phase mismatch can be coupled to the accompanying waveguide through a synthetic phonon bias (Fig. 1A and B). We consider synthetic phonons having angular frequency \( \Omega \), momentum \( q \), and amplitude \( \delta_0 \), which are a modulation of each site’s coupling rate

\[
c_n = c_0 + \delta_0 \cos(\Omega t - q\ell(n - 1))
\]  

(2)

The product \( q\ell \) is equivalent to a phase offset on the modulation applied to adjacent sites; thus, any phonon momentum \( q \) can be selected by modulating each site with a phase offset \( \theta_n = q\ell(n - 1) \). The synthetic phonon bias breaks time-reversal symmetry, and thus induces non-reciprocal coupling, if the momentum \( q \) satisfies \( q\ell = \pm z\pi \), where \( z \) is an integer. This condition is equivalent to having synthetic phonons with a nonzero momentum, since if \( q\ell = \pi \ell \), then a standing wave is formed.

When this spatiotemporally modulated coupling is substituted into Eq. 1, it is instructive to separate the resulting terms into frequency components as follows

\[
C_1 = c_0 \sum_{n=1}^{N} e^{-ik\ell(n-1)} + \frac{\delta_0}{2} e^{i\Omega t} \sum_{n=1}^{N} e^{-ikq\ell(n-1)}
\]

\[
C_2 = c_0 \sum_{n=1}^{N} e^{ik\ell(n-1)} + \frac{\delta_0}{2} e^{-i\Omega t} \sum_{n=1}^{N} e^{ikq\ell(n-1)}
\]

(3)

(4)

For brevity, from here we refer to the terms that make up the coupling constants as \( C_m = C_0^m + C_0^m + C_m^m \) for \( m = 1, 2 \). The first term \( C_0^m \) does not depend on the modulation amplitude \( \delta_0 \) and describes coupling that would occur without synthetic phonons. The remaining terms only describe coupling enabled by interactions with synthetic phonons: \( C_1^m \) corresponds to coupling where a synthetic phonon is annihilated and the photon shifts up in frequency, and \( C_m^m \) corresponds to coupling where a synthetic phonon is created and the photon shifts down in frequency. Because of energy and momentum conservation, both terms incorporate a frequency shift \( (e^{\pm i\Omega t}) \) and momentum shift \( (k \pm q) \), as depicted in Fig. 1A. The momentum shift modifies the original phase matching condition and can enable coupling to a resonator which would otherwise be dark.

Coupling to the resonator, including coupling enabled by the action of synthetic phonons, has a significant impact on wave transmission through the waveguide due to resonant absorption or reflection. In our proposed system, the steady-state forward transmission coefficient \( S_{12} \) as a function of frequency \( \omega \) is evaluated (see the Supplementary Materials for a complete derivation) to be

\[
S_{12} = e^{-i\ell(N-1)\Omega} \frac{C_0^0 C_0^2}{i(\omega - \omega_0) + \gamma} - \frac{C_0^- C_0^+}{i(\omega - \Omega - \omega_0) + \gamma}
\]

(5)

Here, \( S_{12} \) is a linear transfer function, and terms corresponding to transmission with a frequency shift have been dropped. The steady-state backward transmission coefficient \( S_{11} \) is similarly

\[
S_{11} = e^{-i\ell(N-1)\Omega} \frac{C_0^0 C_0^2}{i(\omega - \omega_0) + \gamma} - \frac{C_0^- C_0^+}{i(\omega + \Omega - \omega_0) + \gamma}
\]

(6)

From the above equations, we find that the synthetic phonon-enabled coupling results in a distinct transmission spectrum where resonant absorption can occur at the original resonance frequency \( \omega_0 \) and at the shifted frequencies \( \omega_0 \pm \Omega \). We will hereafter refer to absorption at \( \omega_0 - \Omega \) as the Stokes sideband and absorption at \( \omega_0 + \Omega \) as the anti-Stokes sideband (see Fig. 1A). Since the sideband coupling constants are not required to be equal, that is, \( C_1^+ \neq C_1^- \), transmission at these sidebands can be strongly nonreciprocal. In addition, we note that absorption at the sidebands is in general asymmetric due to the frequency dependence of \( \ell \).

To experimentally validate our theory, we implemented a waveguide-resonator system with three coupling sites \( N = 3 \) using a microstrip waveguide and stub resonator (Fig. 2A, bottom). The fabricated resonator has a loaded resonant frequency \( \omega_0/2\pi \approx 1.4 \) GHz. The waveguide and resonator are coupled through variable capacitors (varactor diodes) which enable dynamic control over the coupling constants \( C_m \) (see Methods). We design the coupling site separation such that \( k\ell = 2\pi/3 \) at \( \omega = \omega_0/2 \), resulting in a complete phase mismatch and creating a dark state. Without a synthetic phonon bias, the measured response for this circuit (Fig. 2A, top) does not indicate any dips in transmission corresponding to resonant absorption, confirming that interactions between the resonator and waveguide are suppressed by the phase mismatch. The broadband background transmission losses are caused by reflection from and losses in the capacitive coupling network.

We next apply synthetic phonons with frequency \( \Omega/2\pi = 104 \) MHz and momentum \( q = -k \) at \( \omega = \omega_0 + \Omega \), implemented through a phase offset \( \theta_n = \frac{2\pi}{\ell} (n - 1) \), to the system, as described by Eq. 2. This phonon momentum was empirically tuned to maximize the coupling rate \( C_1^+ C_2^- \) between the resonator and backward waveguide mode at the anti-Stokes sideband. From Eq. 5, we see that, neglecting any frequency dependence, \( C_1^+ C_2^- \) also describes coupling for the forward waveguide mode at the Stokes sideband. Thus, resonant absorption should occur nonreciprocally: at the anti-Stokes sideband for backward transmission and at the Stokes sideband for forward transmission. The coupling rate \( C_1^+ C_2^- \) is simultaneously minimized by this choice of phonon momentum, so no absorption is expected at these frequencies for the opposite directions (anti-Stokes for forward transmission and Stokes for backward transmission).
The measured forward \( S_{21} \) and backward \( S_{12} \) transmission coefficients for this system are shown in Fig. 2B. As predicted, resonant absorption occurs at \( \approx 1.3 \) GHz only in the forward direction and at \( \approx 1.5 \) GHz only in the backward direction. The frequency dependence of \( k \) creates a slight phase mismatch at the Stokes sideband, resulting in reduced absorption. The measured absorption is highly nonreciprocal, with no resonant absorption observed at \( \approx 1.3 \) GHz in the backward direction or at \( \approx 1.5 \) GHz in the forward direction, validating that \( C^+_1 = C^-_2 \approx 0 \).

In this experiment, we have shown that synthetic phonons can facilitate coupling to dark states by modifying the original phase matching condition. Such phonon-assisted coupling results in nonreciprocal transmission if this modified phase matching condition is not satisfied for both directions simultaneously. However, synthetic phonons that do not modify the phase matching condition, that is, phonons with zero momentum \( (q = 0) \), can also enable coupling to a dark resonator due to the frequency dependence of \( k \). This case, which we show experimentally in Fig. 2C, demonstrates that both waveguide directions can couple to a dark state simultaneously, resulting in reciprocal transmission. We note that because a partial phase mismatch remains, the coupling is weaker at the sidebands and absorption is reduced compared to Fig. 2B.

**Demonstration of elementary nonreciprocal devices**

Nonreciprocal devices such as isolators and circulators are important tools for controlling wave propagation and have a wide range of uses, from protecting lasers against reflections \( (34) \) to facilitating full duplex communications \( (35) \). The gyrator, a fundamental nonreciprocal building block that introduces a unidirectional \( \pi \) phase shift, can be used to produce a variety of nonreciprocal circuits including isolators and circulators. Below, we experimentally show how both isolators and gyrators can be directly created through synthetic phonon–enabled coupling to a single dark state. In addition, in the Supplementary Materials, we provide preliminary experimental evidence of a four-port circulator implemented using synthetic phonon–enabled coupling between a dark state and two waveguides.

We first consider the case of an isolator with high transmission amplitude in the forward direction and zero transmission in the backward direction, operating at the anti-Stokes sideband frequency \( \omega_B + \Omega \). Examining Eqs. 5 and 6, we find that this case occurs when \( C^+_1 C^-_2 = \gamma \) [the critical coupling condition \( (36) \) and \( C^+_1 C^-_2 = 0 \). We experimentally investigated this case using the circuit shown in Fig. 2A. The resonance frequency was tuned to \( \omega_B/2\pi = 1.42 \) GHz, and synthetic phonons were again applied with frequency \( \Omega/2\pi = 104 \) MHz and \( q = -\kappa(\omega_B + \Omega) \). The synthetic phonon amplitude \( \delta_p \) was increased until the critical coupling condition \( C^+_1 C^-_2 = \gamma \) was reached. The measured forward \( S_{21} \) and backward \( S_{12} \) transmission coefficients for synthetic phonons with this critical amplitude are presented in Fig. 3A. We observe a large Lorentzian dip in the measured backward transmission, which drops to below \(-89\) dB at \( 1.52 \) GHz. No resonant absorption is visible in the forward direction. The measured isolation contrast (Fig. 3B) exceeds \( 82\) dB with a \( 10\)-dB bandwidth of approximately \( 12 \) MHz.

We next analyze the case of a gyrator, where high transmission amplitude occurs in both directions, but the backward transmission is phase-shifted by \( \pi \) in comparison to forward transmission. Considering the same system as above, it is evident from Eqs. 5 and 6 that this case occurs if the phonon amplitude is increased such that \( C^+_1 C^-_2 \approx 2\gamma \) (strong overcoupling) while the opposite direction remains uncoupled. We experimentally realize nonreciprocal overcoupling by further increasing the synthetic phonon amplitude such that \( C^+_1 C^-_2 > \gamma \) and observe the anticipated nonreciprocal \( \pi \) phase shift at the anti-Stokes sideband frequency \( \approx 1.52 \) GHz (Fig. 3B). Unfortunately, we were unable to realize the required synthetic phonon amplitude to achieve \( C^+_1 C^-_2 \approx 2\gamma \) due to limitations caused by nonlinearity in the varactor diodes. For comparison, we also show measured transmission amplitude and phase for the...
Fig. 3. Experimental demonstration of essential nonreciprocal functions. Nonreciprocal coupling is enabled by synthetic phonons with the same momentum \( q \) but varying amplitude \( \delta_i \) in all plots. All measurements are focused on the anti-Stokes sideband. (A) Nearly zero transmission (≤92 dB) is measured through the waveguide in the direction that is critically coupled \( |C_1/C_2| = \gamma \). (B) Measured power isolation contrast for the case shown in (A). (C) For an overcoupled resonator, there is a \( \pi \) nonreciprocal phase shift at the anti-Stokes sideband frequency. (D) When the resonator is undercoupled, there is no phase shift at the anti-Stokes sideband frequency.

Fig. 4. Higher-order nonreciprocal transfer functions created through nonreciprocal coupling to resonator networks. (A) Nonreciprocal coupling can be engaged to an arbitrary band-limited impedance network. Several of these impedance networks can be simultaneously coupled in either direction to create customizable responses. (B) Photograph and schematic of the circuit used to demonstrate customizable nonreciprocal transfer functions. (C) Measured power transmission showing a flat band over which a constant isolation response is obtained. (D) Experimental demonstration of four distinct nonreciprocal transfer functions obtained by tuning the resonator network.
undercoupled case, where $C_1^* C_2^- < \gamma$ and there is no nonreciprocal $\pi$ phase shift at the anti-Stokes sideband.

**Higher-order nonreciprocal transfer functions**

While high-order filters are often necessary for signal processing applications (37, 38), a platform for integrating such functionality into nonmagnetic nonreciprocal systems has not yet been shown. Frequency-selective nonreciprocal devices in the literature have been mainly limited to Lorentzian-shaped transfer functions (14, 15, 17–19, 23, 35). Synthetic phonon–enabled coupling is a technique uniquely suited to address this challenge because it can permit unidirectional access to arbitrary band-limited load impedances (Fig. 4A), producing arbitrary nonreciprocal responses. In addition, different frequency responses could be simultaneously achieved in opposite directions by coupling each direction to an appropriate resonator network (39).

Implementing this idea, we experimentally demonstrate non-Lorentzian nonreciprocal transfer functions using the circuit shown in Fig. 4B, which is a modified version of that in Fig. 2A. Here, two additional microstrip stub resonators with tunable resonance frequencies are coupled to the original stub resonator used in previous experiments (Fig. 4B), providing six additional degrees of freedom: the additional resonance frequencies $\omega_1$, $\omega_2$, interresonator coupling rates $k_1$, $k_2$, and linewidths $\gamma_1$, $\gamma_2$.

A maximally flat nonreciprocal filter with constant isolation over an appreciable bandwidth is arguably one of the most important functionalities that cannot be implemented using a single resonant response. Such a flat response can be approximated in the three-resonator network using $\gamma_1 = \gamma_2 = \gamma$, $k_1 = k_2 = 9\gamma/14$, $\omega_1 = \omega_0 + 3\gamma/7$, and $\omega_2 = \omega_0 - 3\gamma/7$, where the loss rate $\gamma$ and resonance frequency $\omega_0$ are associated with the original resonator. We empirically tuned both the resonance frequencies ($\omega_1$, $\omega_2$) and coupling rates ($k_1$, $k_2$) of the additional resonators in our circuit (Fig. 4B) near these values until the desired transfer function was achieved. Since the resonators are fabricated on the same substrate and conductor, their linewidths are intrinsically equal. The experimentally measured transmission through the waveguide (Fig. 4C) exhibits nearly constant isolation of 14 dB over a 10-MHz bandwidth. In Fig. 4D, we present four additional examples of arbitrary nonreciprocal transfer functions obtained by varying the interresonator coupling strength and frequency separation of the three resonators. In these experiments, we observe consistently flat forward transmission ($S_{21}$) even though the reverse transmission ($S_{12}$) varies, demonstrating that propagation in the uncoupled direction is largely unaffected by changes to the impedance network.

**DISCUSSION**

Here, we have demonstrated that coupling to arbitrary networks of resonators can be engaged nonreciprocally, and have used such coupling to realize new higher-order nonreciprocal filters and fundamental nonreciprocal devices. Furthermore, we have introduced synthetic phonons with a precisely controlled momentum, which can replicate the action of optically active phonons without relying on any dispersion relation. Although our experiments take place in microstrip circuits, the nonreciprocal behavior of our system is captured by coupled-mode theory, and thus, the underlying method can be extended to a wide variety of physical systems. In addition, the concept of nonreciprocal coupling can be applied broadly to a number of band-limited devices besides resonators, including antennas, amplifiers, oscillators, and sensors, allowing the creation of highly customizable integrated devices.

**METHODS**

**Experimental setup**

Our microwave circuits were fabricated on Rogers RT/duroid 5880 substrate with a 1-oz copper conductor and consist of a microstrip waveguide coupled to a ring resonator by N varactor diodes (Skyworks SMV1275) that acted as variable capacitors. The coupling strength $c_n$ of each capacitive Coupler is an approximately linear function of the applied voltage $V_n$ (for small changes), allowing a modulation of $c_n$ that is proportional to a modulation of $V_n$. We first applied a dc bias to each varactor diode with a dc power supply (Agilent E3631A), which lowered the capacitance and decreased the background reflection caused by the coupling system. On top of this bias, we applied a small sinusoidal signal from a signal generator (HP-8647B), which was set at a frequency of 104 MHz. This signal was split (Minicircuits ZA3CS-400-3W-S) into three variable phase shifters (Minicircuits JSPHS-150+) so that the phase shift between each signal could be independently controlled. The DC bias and three 104-MHz modulation signals were combined through three bias tees (Minicircuits ZFBFT-4R2GW-F+) and connected directly to the circuit through the ports labeled Bias in Fig. 2. On each circuit, butterfly band-pass filters were incorporated along with another low-frequency biasing tee (Johanson Technology L-14C10N-V4T 10 nH inductor and Johanson Technology R14S 6.8 pF capacitor), as shown in Fig. 2, to isolate the lower-frequency (104 MHz) bias modulation from the higher-frequency ($\approx$1.4 GHz) resonant circuit.

**Measurement**

We measured the transmission parameters ($S_{21}, S_{12}$) of the circuit using a Keysight E5063A vector network analyzer. The network analyzer measurement was calibrated to the ends of the coaxial cables that connected to the surface-mount SubMiniature version A (SMA) connectors on the circuit board. Thus, the data presented throughout this paper only reflect the $S$ parameters of the circuits that we have developed, while eliminating any parasitic effects from the cables and supporting systems.

**SUPPLEMENTARY MATERIALS**

Supplementary material for this article is available at http://advances.sciencemag.org/cgi/content/full/4/6/eaat0232/DC1

section 51. Steady-state transmission coefficients
section 52. Resonant decay rate
section 53. Circulator
fig. 51. Schematic of a waveguide-resonator system with one resonance and two ports.
fig. 52. Theoretical description of a circulator implemented with nonreciprocal coupling.
fig. 53. Experimentally measured circulator implemented with nonreciprocal coupling.

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