LiSHT: Non-Parametric Linearly Scaled Hyperbolic Tangent Activation Function for Neural Networks

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Abstract. The activation function in neural network introduces the non-linearity required to deal with the complex tasks. Several activation/non-linearity functions are developed for deep learning models. However, most of the existing activation functions suffer due to the dying gradient problem and non-utilization of the large negative input values. In this paper, we propose a Linearly Scaled Hyperbolic Tangent (LiSHT) for Neural Networks (NNs) by scaling the Tanh linearly. The proposed LiSHT is non-parametric and tackles the dying gradient problem. We perform the experiments on benchmark datasets of different type, such as vector data, image data and natural language data. We observe the superior performance using Multi-layer Perceptron (MLP), Residual Network (ResNet) and Long-short term memory (LSTM) for data classification, image classification and tweets classification tasks, respectively. The accuracy on CIFAR100 dataset using ResNet model with LiSHT is improved by 9.48, 3.40, 3.16, 4.26, and 1.17\% as compared to Tanh, ReLU, PReLU, LReLU, and Swish, respectively. We also show the qualitative results using loss landscape, weight distribution and activations maps in support of the proposed activation function.

Keywords: Activation Function · Convolutional Neural Networks · Non-Linearity · Tanh function · Image Classification.

1 Introduction

The deep learning method is one of the breakthroughs which replaced the hand-tuning tasks in many problems including computer vision, speech processing, natural language processing, robotics, and many more\textsuperscript{[28], [9], [29], [4], [8]}. In recent times, the deep Artificial Neural Networks (ANNs) have shown a tremendous performance improvement due to existence of larger datasets as well as powerful computers\textsuperscript{[12]}. Various types of ANN have been proposed for several problems such as Multilayer Perceptron (MLP)\textsuperscript{[17]} to deal with the real vector $\mathbb{R}$-dimensional data\textsuperscript{[13]}. Convolutional Neural Networks (CNN) are used to deal with the image and video\textsuperscript{[14]}. Recurrent Neural
Network (RNN) like Long-Short Term Memory (LSTM) are used for the sentiment analysis [30]. The main aim of different type of neural networks is to transform the input data in abstract feature space. In order to achieve it, all the neural networks rely on a compulsory unit called the activation function [1]. The activation functions bring the non-linear capacity in the network to deal with the complex data [2].

The Sigmoid activation function was mostly used in the at the inception of neural networks. It is a special case of the logistic function. The Sigmoid function squashes the real-valued numbers into 0 or 1. In turn, the large negative number becomes 0 and large positive number becomes 1. The hyperbolic tangent function Tanh is the another popular activation function. The output range of Tanh is defined with \(-1\) as lower limit and \(1\) as upper limit. The vanishing gradient in both positive as well as negative directions is one of the major problems with both Sigmoid and Tanh activation functions. The Rectified Linear Unit (ReLU) activation function was proposed in recent past for training deep networks [22]. ReLU is a breakthrough against vanishing gradient. It is a zero function (i.e., the output is zero) for the negative inputs and an identity function for the positive inputs. The ReLU is very simple, hence became very popular and mostly used in different deep models. The diminishing gradient for the inputs less than zero can be seen as primary bottleneck with ReLU leading to dying gradient problem.

Several researchers have proposed the improvement on ReLU such as Leaky ReLU (LReLU) [25], Parametric ReLU (PReLU) [13], Softplus [26], Exponential Linear Unit (ELU) [3], Scaled Exponential Linear Unit (SELU) [20], Gaussian Error Linear Unit (GELU) [16], Average Biased ReLU (ABReLU) [5], Linearized sigmoidal activation (LiSA) [2] etc. The ReLU is extended to LReLU by allowing a small, non-negative and constant gradient (such as 0.01) for the negative inputs [25]. The PReLU makes the slopes of linear function for negative inputs (i.e., leaky factor) as trainable [13]. The Softplus activation function tries to make the transition of ReLU (i.e., at 0) smooth by fitting the log function [26]. Otherwise, the Softplus activation is very similar to the ReLU activation. The ELU function is same as ReLU for positive inputs and exponential for negative inputs [3]. The ELU becomes smoother near zero. For positive inputs, the ELU [3] can blow up the activation, which can lead to the gradient exploding problem. The SELU adds one scaling parameter in ELU, which makes it better against weight initialization [20]. The GELU uses a Gaussian approach to apply the zero/identity map to the input of a unit randomly [16]. The ABReLU utilizes the representative negative values as well as representative positive values by shifting rectification based on the average of activation values [5]. The ABReLU also could not utilize all the negative values due to trimming of values at zero, similar to ReLU. Most of these existing activation methods are sometimes not able to take the advantage of negative values which is solved in the proposed LiSHT activation.

Recently, Xu et al. have performed an empirical study of rectified activations in CNNs [31]. Very recently, a promising Swish activation function was introduced as sigmoid-weighted linear unit, i.e., \(f(x) = x \times \text{sigmoid}(\beta x)\) [27]. Based on the value of the learnable \(\beta\), Swish adjusts the amount of non-linearity.

In this paper, a linearly scaled hyperbolic tangent activation function (LiSHT) is proposed to introduce the non-linearities in the neural networks. The LiSHT scales the Tanh function linearly to tackle its gradient diminishing problem.
The contributions of this paper are as follows,

- A new activation function named non-parametric LinearlyScaled Hyperbolic Tangent (LiSHT) is proposed by linearly scaling the Tanh activation function.
- The increased amount of non-linearity of the proposed activation function is visualized from its first and second order derivatives curves (Fig. 1).
- The proposed LiSHT activation function is tested with different types of neural networks, including Multilayer Perceptron, Residual Neural Network, and Long-Short Term Memory based networks.
- Three different types of experimental data are used 1) $\mathbb{R}$-dimensional data, including Iris and MNIST (converted from image) datasets, 2) image data, including MNIST, CIFAR-10 and CIFAR-100 datasets, and 3) sentiment analysis data, including twitter140 dataset.
- The impact of different non-linearity functions over activation feature maps and weight distribution has been analyzed.
- The activation maps, weight distributions and optimization landscape are also analyzed to show the effectiveness of the proposed LiSHT activation function.

This paper is organized as follows: Section 2 outlines the proposed LiSHT activation; Section 3 presents the mathematical analysis; Section 4 describes the experimental setup; Section 5 presents the results; and Section 6 contains the concluding remarks.

### 2 Proposed LiSHT Activation Function

A Deep Neural Network (DNN) comprises of multiple hidden nonlinear layer. Let an input vector be $x \in \mathbb{R}^d$, and each layer transforms the input vector followed by a nonlinear mapping from the $l^{th}$ layer to the $(l+1)^{th}$ layer as follows:

\[
\begin{align*}
\tau^0 & = x \\
\tau_{l+1} & = \sum_{j=1}^{N^l} w_{ij}^l \tau_j^l + d_i^l \\
\tau_j^l & = \phi(s_j^{l+1})
\end{align*}
\]
Here, $\tau$ represents the activation volume of any given layer, $s_i^l$, $w_{ij}^l$, $o_i^l$, and $N^l$ represent the vectors of output, weights, biases and number of units in the hidden $l^{th}$ layer, respectively, and a non-linear activation mapping $\phi(x)$. Looking for an efficient and powerful activation function in DNN is always demanding due to the overabundance by the saturation properties of existing activation functions. An activation function $\phi(x)$ is said to be saturate [10], if its derivative $\phi'(x)$ tends to zero in both directions (i.e., $x \to \infty$ and $x \to -\infty$, respectively). The training of a deep neural networks is almost impossible with of Sigmoid and Tanh activation functions due to the gradient diminishing problem when input is either too small or too large [12]. For the first time, the Rectified Linear Unit (ReLU) (i.e., $\phi(x) = \max(0, x)$) became very popular activation for training the DNN [22]. But, ReLU also suffers due to the gradient diminishing problem for negative inputs which lead to the dying neuron problem.

Hence, we propose a non-parametric linearly scaled hyperbolic tangent activation function, so called LiSHT. Like ReLU [22] and Swish [27], LiSHT shares the similar unbounded upper limits property on the right hand side of activation curve. However, because of the symmetry preserving property of LiSHT, the left hand side of the activation is in the upwardly unbounded direction, hence it satisfies non-monotonicity (see Fig. 1(a)). Apart from the literature [3],[27] and to the best of our knowledge, first time in the history of activation function, LiSHT utilizes the benefits of positive valued activation without identically propagating all the inputs, which mitigates gradient vanishing at back propagation and acquiesces faster training of deep neural network. The proposed activation function LiSHT is computed by multiplying the $\text{Tanh}$ function to its input $x$ and defined as,

$$\phi(x) = x \cdot g(x)$$

(2)

where $g(x)$ is a hyperbolic tangent function and defined as,

$$g(x) = \text{Tanh}(x) = \frac{e^{x} - e^{-x}}{e^{x} + e^{-x}}.$$  

(3)

where $x$ is the input to the activation function and $\exp$ is the exponential function.

For the large positive inputs, the behavior of the LiSHT is close to the ReLU and Swish, i.e., the output is close to the input as depicted in Fig. 1(a). Whereas, unlike ReLU and other commonly used activation functions, the output of LiSHT for negative inputs is symmetric to the output of LiSHT for positive inputs as illustrated in Fig. 1(a). The $1^{st}$ order derivative (i.e., $\phi'(x)$) of LiSHT is given as follows,

$$\phi'(x) = x[1 - \text{Tanh}^2(x)] + \text{Tanh}(x)$$

$$= x + \text{Tanh}(x)[1 - \phi(x)].$$

(4)

Similarly, the $2^{nd}$ order derivative (i.e., $\phi''(x)$) of LiSHT is given as follows,

$$\phi''(x) = 1 - \text{Tanh}(x)\phi(x) + [1 - \phi(x)](1 - \text{Tanh}^2(x))$$

$$= 2 - \text{Tanh}(x)\phi'(x) - \phi(x) - \text{Tanh}(x)[\phi'(x) - x]$$

$$= 2[1 - \text{Tanh}(x)\phi'(x)].$$

(5)
The 1st and 2nd order derivatives of the proposed *LiSHT* are plotted in Fig. 1(b) and Fig. 1(c), respectively. An attractive characteristic of the *LiSHT* is self-stability property, the magnitude of derivatives is less than 1 for $x \in [-0.65, 0.65]$. It can be observed from the derivatives of *LiSHT* in Fig. 1 that the amount of non-linearity is very high near to zero as compared to the existing activations which can boost the learning of a complex model. As described in Fig. 1(c) that the 2nd order derivative of proposed *LisHT* activation function is similar to the opposite of the Laplacian operator (i.e., the 2nd order derivative of Gaussian operator) which is useful to maximize a function. Thus, due to opposite nature of Gaussian operator, the proposed *LiSHT* activation function boosts the training of the neural network for the minimization problem of the loss function.

We understand that being unbounded for both negative and positive inputs, smooth, and non-monotonicity are the advantages of the proposed *LiSHT* activation. The complete unbounded property makes *LiSHT* different from all the traditional activation functions. Moreover, it makes use of strong advantage of positive feature space. *LiSHT* is a smooth, symmetric w.r.t. y-axis and non-monotonic function and introduces more amount of non-linearity in the training process than *Swish*.

### 3 Mathematical Analysis

In this section we show mathematically that *LiSHT* actively solves the vanishing gradient problem of *Tanh*. The flow of gradient through any activation function is depicted in Fig. 2. Let $\phi$ is an activation function given as $z = \phi(x)$, where $x$ is the input and $z$ is the output. Let $L$ is the final objective function and the running gradient $\frac{\partial L}{\partial z}$ is the input to $\phi$ during back-propagation. The running gradient output of $\phi$ is $\frac{\partial L}{\partial x} = \frac{\partial L}{\partial z} \cdot \frac{\partial z}{\partial x}$ using chain rule, where $\frac{\partial z}{\partial x}$ is the local gradient of $\phi$.

**Theorem 1.** If $\phi = Tanh$ then it leads to the gradient diminishing problem.

**Proof.**

$$z = \text{Tanh}(x)$$  \hspace{1cm} (6)

The local gradient for *Tanh* activation is given as,

$$\frac{\partial z}{\partial x} = 1 - \text{Tanh}^2(x) \approx \begin{cases} 0, & x < -2 \\ \frac{2x}{2}, & -2 \leq x \leq 2 \\ 0, & x > 2 \end{cases}$$  \hspace{1cm} (7)
where $\tanh^2(x) \approx 1$ for $-2 < x < 2$. It can be noticed that for smaller and larger inputs the local gradient $\frac{\partial z}{\partial x}$ of $\tanh$ is very close to zero which makes the running gradient $\frac{\partial L}{\partial x}$ also close to zero, thus leading to the gradient diminishing problem.

**Theorem 2.** If $\phi = \text{LiSHT}$ then the local gradient $\frac{\partial z}{\partial x} = 0$ iff $x = 0$.

**Proof.**

$$z = \text{LiSHT}(x) = x \cdot \tanh(x) \quad (8)$$

The local gradient for LiSHT activation is given as,

$$\frac{dz}{dx} = x + \tanh(x)[1 - x\tanh(x)] \quad (9)$$

For $x < -2$, $\tanh(x) \approx -1$, thus $\frac{\partial z}{\partial x} \approx -1$. For $x > 2$, $\tanh(x) \approx 1$, thus $\frac{\partial z}{\partial x} \approx 1$. For $-2 \leq x \leq 2$, $-1 \leq \tanh(x) \leq 1$, thus $2x - 1 \leq \frac{\partial z}{\partial x} \leq 2x + 1$. The LiSHT can lead to gradient diminishing problem iff $\frac{\partial z}{\partial x} = x + \tanh(x)[1 - x\tanh(x)] = 0$. It means $x = \frac{\tanh(x)}{\tanh^2(x) - 1}$, which is only possible iff $x = 0$. It can be also visualized in Fig. [b]. Thus, the *LiSHT* activation function exhibits non-zero gradient for all positive and negative inputs and solves the gradient diminishing problem of $\tanh$ activation function.

## 4 Experimental Setup

In this section, first, six datasets are described in detail, then the three types of networks are summarized, and finally the training settings are stated in detail.

### 4.1 Datasets Used

We evaluate the proposed *LiSHT* activation function on five benchmark databases, including Iris, MNIST, CIFAR-10, CIFAR-100 and twitter140. The *Fisher’s Iris Flower dataset* [32] consists three Iris species (i.e., Versicolor, Virginica and Setosa) with a total of 150 examples. Each example of Iris dataset is represented by four characteristics, including length and width of petal and sepal, respectively. The *MNIST dataset* is a popular dataset to recognize the English digits (i.e., 0 to 9) in images. It consists of 60,000 and 10,000 images in the training and test sets, respectively [23]. The *CIFAR-10 dataset* is an object recognition dataset with 10 categories having images of resolution $32 \times 32$ [21]. The 50,000 and 10,000 images are available in the training and test sets, respectively. All the images of the CIFAR-10 dataset are also present in the *CIFAR-100 dataset* (i.e., 50K for training and 10K for testing), but categorized in 100 classes. The training and testing test sets contain 100 classes in CIFAR-100 dataset. The *twitter140 dataset* [11] is used to perform the classification of sentiments of Twitter messages by classifying as either positive, negative or neutral with respect to a query. In this dataset, we have considered 1,600,000 examples, where 85% are used as training set and the rest 15% as validation set.

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#### 4.2 Tested Neural Networks

We use three models, including a Multi-layer Perceptron (MLP), a widely used Pre-activated Residual Network (ResNet-PreAct) \[15\], and a Long-Short Term Memory (LSTM) to show the performance of activation functions. These architectures are explained in this section. The **Multi-layer Perceptron (MLP)** with one hidden layer is used in this paper for the classification of data. The internal architecture in MLP uses input, hidden and final **softmax** layer with 6, 5, and 4 nodes for the Car evaluation dataset. For Iris Flower dataset, the MLP uses 4, 3, and 3 nodes in the input, hidden and final **softmax** layer, respectively. The MNIST dataset samples are converted into 1-D vectors when used with MLP. Thus, for MNIST dataset, the MLP uses 784 neurons in the input layer, 512 neurons in the hidden layer, and 10 neurons in the last layer. The **Residual Neural Network (ResNet)** is a very popular CNN model for the image classification task. We use the Pre-activated ResNet \[15\] for image classification experiments in this paper. The ResNet-PreAct is used with 164-layer (i.e., very deep network) for CIFAR-10 and CIFAR-100 datasets, whereas it is used with 20-layer for MNIST dataset. The channel pixel mean subtraction is used for preprocessing over image datasets with this network as per the standard practice being followed by most image classification neural networks. In this paper, the **Long Short Term Memory (LSTM)** is used as the third type of neural network, which basically belongs to the Recurrent Neural Network (RNN) family. A single layered LSTM with 196 cells is used for sentiment analysis over twitter140 dataset. The LSTM is fed with 300 dimensional word vectors trained with FastText Embeddings.

#### 4.3 Training Settings

We perform the implementation using in the Keras deep learning framework. Different computer systems, including different GPUs (such as NVIDIA Titan X, Pascal 12GB GPU and NVIDIA Titan V 12GB GPU) are used at different stages of the experiments.

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**Table 1**: The classification accuracy on Iris and MNIST datasets using different activation functions for MLP model.

| Dataset | Sigmoid | Tanh | ReLU \[22\] | PReLU \[13\] | LReLU \[25\] | Swish \[27\] | LiSHT |
|---------|---------|------|-------------|-------------|-------------|-------------|-----|
| Iris    | 96.23   | 96.26| 96.41       | 97.11       | 96.53       | 96.34       | **97.33** |
| MNIST   | 98.43   | 98.26| 98.48       | 98.34       | 97.69       | 98.45       | **98.60** |

**Table 2**: The classification accuracy on MNIST and CIFAR-10/100 datasets using different activation functions for ResNet model.

| Dataset | ResNet Depth | Tanh | ReLU \[22\] | PReLU \[13\] | LReLU \[25\] | Swish \[27\] | LiSHT |
|---------|--------------|------|-------------|-------------|-------------|-------------|-----|
| MNIST   | 20           | 99.48| 99.56       | 99.56       | 99.52       | 99.53       | **99.59** |
| CIFAR-10| 164          | 89.74| 91.15       | 92.86       | 91.50       | 91.60       | **92.92** |
| CIFAR-100| 164        | 68.80| 72.84       | 73.01       | 72.24       | 74.45       | **75.32** |
Table 3: The classification accuracy on twitter140 dataset using different activation functions for LSTM model.

| Dataset    | Activation Functions |
|------------|----------------------|
|            | Tanh     | ReLU [22] | LReLU [25] | Swish [27] | LiSHT    |
| Twitter140 | 82.27    | 82.47     | 78.18      | 82.22      | 82.47    |

The Adam optimizer [19,6] is used for the experiments in this paper. The batch size is set to 128 for the training of the networks. The learning rate is initialized to 0.1 and reduced by a factor of 0.1 at 80th, 120th, 160th, and 180th epochs during training. For LSTM, after 10625 iteration on 128 sized mini-batches, the learning rate is dropped by a factor of 0.5 up to 212, 500 mini-batch iterations.

5 Results and Analysis

We investigate the performance and effectiveness of the proposed LiSHT activation and compare with state-of-the-art activation functions such as Tanh, ReLU, and Swish.

5.1 Experimental Results

The results on Iris and MNIST datasets using MLP model are reported in Table 1. The categorical cross-entropy loss is used to train the models for 200 epochs. In order to run training smoothly in both the dataset, 80% of samples were randomly chosen for training and remaining 20% are used for validation. The proposed LiSHT activation achieves outperforms the existing activation functions. The top accuracy on Iris and MNIST datasets are achieved by LiSHT as 97.33% and 98.60%, respectively.

Table 2 shows the validation accuracies on MNIST, CIFAR-10 and CIFAR-100 datasets for different activations with pre-activation ResNet. The depth of ResNet is 20 for MNIST and 164 for CIFAR datasets. We train the model for 200 epochs using the cross-entropy objective function. It is observed that LiSHT outperforms the other activation functions on MNIST, CIFAR-10 and CIFAR-100 datasets, and achieves 99.59% and 92.92%, and 75.32% accuracy, respectively. Moreover, a significant improvement has been shown by LiSHT on CIFAR datasets. The unbounded, symmetric and more non-linear properties of the proposed LiSHT activation function facilitates better and efficient training as compared to the other activation functions such as Tanh, ReLU and Swish. The unbounded and symmetric nature of LiSHT leads to the more exploration of weights and positive and negative gradients to tackle the gradient diminishing and exploding problems.

The sentiment classification performance in terms of the validation accuracy is reported in Table 3 over twitter140 dataset with LSTM for different activations. It is observed that the performance of proposed LiSHT activation function is better than Tanh and Swish, whereas the same as ReLU. It points out one important observation that by considering the negative values as negative by Swish degrades the performance because it leads the Swish activation more towards the linear function as compared to the ReLU activation.
5.2 Result Analysis

The convergence curve of losses is also used as the metric to measure the learning ability of the ResNet model with different activation functions. The training and validation loss over the epochs are plotted in Fig. 3 and 4 for MNIST, CIFAR-10 and CIFAR-100 datasets using ResNet. It is clearly observed that the proposed LiSHT boosts the convergence speed. It is also observed that the LiSHT outperforms the existing non-linearities across several classification tasks with MLP, ResNet and LSTM networks.

5.3 Analysis of Activation Feature Maps

In deep learning, it is a common practice to visualize the activations of different layer of the network. In order to understand the effect of activation functions over the learning of important features at different layer, we have shown the activation feature maps for different non-linearities at $2^{nd}$ layer of the pre-activation ResNet of MNIST digit 7 in Fig. 5. The number of activation feature maps in $2^{nd}$ and $11^{th}$ layers are 64 (each having the $32 \times 32$ spatial dimensions) and 128 (each having the $16 \times 16$ spatial dimensions), respectively. It can be seen from Fig. 5 that the images looking deeper blue are due
to the dying neuron problem caused by the non-learnable behavior arose due to the improper handling of negative values by the activation functions. The proposed LiSHT activation consistently outperforms other activations. It is observed that the LiSHT generates the less number of non-learnable filters due to the unbounded nature in both positive and negative scenarios which helps it to overcome from the problem of dying gradient. It is also observed that some image patches contain noise in terms of the Yellow color. The patches corresponding to the LiSHT contain less noise. Moreover, it is uniformly distributed over all the patches, when LiSHT is used, compared to other activation functions. It may be also one of the factors that proposed LiSHT outperforms other activations.

5.4 Analysis of Final Weight Distribution

The weights of the layers are useful to visualize because it gives the idea about the learning pattern of the network in terms of 1) the positive and negative biasedness and 2) the exploration of weights caused by the activation functions. We have portrayed the weight distribution of final Conv layer in Fig. 6 for pre-activation ResNet over the MNIST dataset using Tanh, ReLU, Swish and LiSHT activations. The weight distri-
Fig. 5: Visualization of MNIST digit 7 from the 2nd conv layer activation feature maps without feature scale clipping using a fully trained pre-activation ResNet model using the (a) Tanh (b) ReLU (c) Swish and (d) LiSHT activation, respectively. Note that there are 64 feature maps of dimension 32 × 32 in the 2nd layer, represented in 4 rows and 16 columns.

Fig. 6: Visualizations of the distribution of weights from the final Conv layer of pre-activation ResNet over MNIST dataset for the (a) Tanh (b) ReLU (c) Swish and (d) LiSHT activations, respectively.

bution for Tanh is limited in between −5 and 4 (see 6(a)) due to its bounded nature in both negative and positive regions. Interestingly, as depicted in 6(b), the weight distribution for ReLU is biased towards the positive region because it converts all negative values to zero which restricts the learning of weights in the negative direction. This leads to the problems of dying gradient as well as gradient exploding. The Swish tries to overcome the problems of ReLU, but unable to succeed due to the bounded nature in
5.5 Analysis of Loss Landscape

The training ability of DNN is directly and indirectly influenced by the factors like network architecture, the choice of optimizer, variable initialization, and most importantly, what kind of non-linearity function to be used in the architecture. In order to understand the effects of network architecture on non-convexity, we trained the ResNet-152 using ReLU, Swish and proposed LiSHT activations and try to explore the structure of the neural network loss landscape. The 2D and 3D visualizations of loss landscapes are illustrated in Fig. 7 and 8 by following the visualization technique proposed by Li et al. [24].

As depicted in the 2D loss landscape visualizations in Fig. 7(a)-(c), the LiSHT makes the network to produce the smoother loss landscapes with smaller convergence steps which is populated by the narrow, and convex regions. It directly impacts the loss landscape. However, Swish and ReLU also produce smooth loss landscape with large convergence steps, but unlike LiSHT, both Swish and ReLU cover wider searching
area which leads to poor training behavior. In 3D landscape visualization, it can be seen in Fig. 8(a)-(c), it can be observed that the slope of the LiSHT loss landscape is higher than the Swish and ReLU which enables to train deep network efficiently. Therefore, we can say that, the LiSHT decreases the non-convex nature of overall loss minimization landscape as compared to the ReLU and Swish activation functions.

6 Conclusion

A novel non-parametric linearly scaled hyper tangent activation function (LiSHT) is proposed in this paper for training the neural networks. The proposed LiSHT activation function introduces more non-linearity in the network. It is completely unbounded and solves the problems of diminishing gradient problems. Other properties of LiSHT are symmetry, smoothness and non-monotonicity, which play an important roles in training. The classification results are compared with the state-of-the-art activation functions. The efficacy of LiSHT is tested on benchmark datasets using MLP, ResNet and LSTM models. The experimental results confirm the effectiveness of the unbounded, symmetric and highly non-linear nature of the proposed LiSHT activation function. The importance of unbounded and symmetric non-linearity in both positive and negative regions are analyzed in terms of the activation maps and weight distribution of the learned network. The visualization of loss landscape confirms the effectiveness of the proposed activations to make the training more smoother with faster convergence.

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References

1. Agostinelli, F., Hoffman, M., Sadowski, P., Baldi, P.: Learning activation functions to improve deep neural networks. arXiv preprint arXiv:1412.6830 (2014)
2. Bawa, V.S., Kumar, V.: Linearized sigmoidal activation: A novel activation function with tractable non-linear characteristics to boost representation capability. Expert Systems with Applications 120, 346–356 (2019)
3. Clevert, D.A., Unterthiner, T., Hochreiter, S.: Fast and accurate deep network learning by exponential linear units (elus). arXiv preprint arXiv:1511.07289 (2015)
4. Dubey, S.R.: A decade survey of content based image retrieval using deep learning. IEEE Transactions on Circuits and Systems for Video Technology 32(5), 2687–2704 (2021)
5. Dubey, S.R., Chakraborty, S.: Average biased relu based cnn descriptor for improved face retrieval. Multimedia Tools and Applications 80(15), 23181–23206 (2021)
6. Dubey, S.R., Chakraborty, S., Roy, S.K., Mukherjee, S., Singh, S.K., Chaudhuri, B.B.: diffgrad: An optimization method for convolutional neural networks. IEEE Transactions on Neural Networks and Learning Systems (2019)
7. Dubey, S.R., Singh, S.K., Chaudhuri, B.B.: Activation functions in deep learning: A comprehensive survey and benchmark. Neurocomputing (2022)
8. Dubey, S.R., Singh, S.K., Chu, W.T.: Vision transformer hashing for image retrieval. In: 2022 IEEE International Conference on Multimedia and Expo (ICME). pp. 1–6. IEEE (2022)
9. Garcia-Garcia, A., Orts-Escolano, S., Oprea, S., Villena-Martinez, V., Garcia-Rodriguez, J.: A review on deep learning techniques applied to semantic segmentation. arXiv preprint arXiv:1704.06857 (2017)
10. Glorot, X., Bordes, A., Bengio, Y.: Deep sparse rectifier neural networks. Proceedings of the fourteenth international conference on artificial intelligence and statistics pp. 315–323 (2011)
11. Go, A., Bhayani, R., Huang, L.: Twitter sentiment classification using distant supervision. Technical report, Stanford (2009)
12. Goodfellow, I., Bengio, Y., Courville, A., Bengio, Y.: Deep learning, vol. 1. MIT press Cambridge (2016)
13. He, K., Zhang, X., Ren, S., Sun, J.: Delving deep into rectifiers: Surpassing human-level performance on imagenet classification. Proceedings of the IEEE international conference on computer vision pp. 1026–1034 (2015)
14. He, K., Zhang, X., Ren, S., Sun, J.: Deep residual learning for image recognition. Proceedings of the IEEE conference on computer vision and pattern recognition pp. 770–778 (2016)
15. He, K., Zhang, X., Ren, S., Sun, J.: Identity mappings in deep residual networks. European conference on computer vision pp. 630–645 (2016)
16. Hendrycks, D., Gimpel, K.: Bridging nonlinearities and stochastic regularizers with gaussian error linear units. arXiv preprint arXiv:1606.08415 (2016)
17. Hornik, K., Stinchcombe, M., White, H.: Multilayer feedforward networks are universal approximators. Neural networks 2(5), 359–366 (1989)
18. Kim, L.W.: Deepx: Deep learning accelerator for restricted boltzmann machine artificial neural networks. IEEE transactions on neural networks and learning systems 29(5), 1441–1453 (2018)
19. Kingma, D.P., Ba, J.: Adam: A method for stochastic optimization. arXiv preprint arXiv:1412.6980 (2014)
20. Klambauer, G., Unterthiner, T., Mayr, A., Hochreiter, S.: Self-normalizing neural networks. Advances in Neural Information Processing Systems pp. 971–980 (2017)
21. Krizhevsky, A.: Learning multiple layers of features from tiny images. Tech. rep., Citeseer (2009)
22. Krizhevsky, A., Sutskever, I., Hinton, G.E.: Imagenet classification with deep convolutional neural networks. Advances in neural information processing systems pp. 1097–1105 (2012)
23. LeCun, Y., Bottou, L., Bengio, Y., Haffner, P.: Gradient-based learning applied to document recognition. Proceedings of the IEEE 86(11), 2278–2324 (1998)
24. Li, H., Xu, Z., Taylor, G., Studer, C., Goldstein, T.: Visualizing the loss landscape of neural nets. Advances in Neural Information Processing Systems pp. 6389–6399 (2018)
25. Maas, A.L., Hannun, A.Y., Ng, A.Y.: Rectifier nonlinearities improve neural network acoustic models. Proc. icml 30(1), 3 (2013)
26. Nair, V., Hinton, G.E.: Rectified linear units improve restricted boltzmann machines. Proceedings of the 27th international conference on machine learning (ICML-10) pp. 807–814 (2010)
27. Ramachandran, P., Zoph, B., Le, Q.V.: Swish: a self-gated activation function. arXiv preprint arXiv:1710.05941 (2017)
28. Schmidhuber, J.: Deep learning in neural networks: An overview. Neural networks 61, 85–117 (2015)
29. Voulodimos, A., Doulamis, N., Doulamis, A., Protopapadakis, E.: Deep learning for computer vision: A brief review. Computational intelligence and neuroscience 2018 (2018)
30. Wang, Y., Huang, M., Zhao, L., et al.: Attention-based lstm for aspect-level sentiment classification. Proceedings of the 2016 conference on empirical methods in natural language processing pp. 606–615 (2016)
31. Xu, B., Wang, N., Chen, T., Li, M.: Empirical evaluation of rectified activations in convolutional network. arXiv preprint arXiv:1505.00853 (2015)
32. Zhang, L., Suganthan, P.N.: Random forests with ensemble of feature spaces. Pattern Recognition 47(10), 3429–3437 (2014)