Land-Use Conversion Changes the Multifractal Features of Particle-Size Distribution on the Loess Plateau of China

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Abstract: Analyzing the dynamics of soil particle-size distributions (PSDs), soil nutrients, and erodibility are very important for understanding the changes of soil structure and quality after long-term land-use conversion. We applied multifractal Rényi spectra ($D_q$) and singularity spectra ($f(\alpha)$) to characterize PSDs 35 years after conversions from cropland to shrubland with Caragana microphylla (shrubland I), shrubland with Hippophae rhamnoides (shrubland II), forested land, and grassland on the Loess Plateau of China. Multifractal parameters (capacity dimension ($D_0$), entropy dimension ($D_1$), $D_1/D_0$, correlation dimension ($D_2$), and Hölder exponent of order zero ($\alpha_0$)) were used to analyze the changes of PSDs. $D_q$ and $f(\alpha)$ characterized the PSDs well and sensitively represented the changes in PSDs after conversion. All types of land-use conversion significantly improved the properties of the topsoil (0–10 cm), but the effect of shrubland I and even forested land decreased with depth. All types of land-use conversion significantly increased $D_1$ and $D_2$ in the topsoil, and $D_1$ and $D_2$ in the 10–50 cm layers of shrubland II, forested land, and grassland and $D_1$ in the 50–100 cm layers of shrubland II were significantly higher relative to the control. Both $D_1$ and $D_2$ were positively correlated with the contents of soil nutrients and fine particles and were negatively correlated with soil erosion, indicating that $D_1$ and $D_2$ were potential indices for quantifying changes in soil properties and erosion. In conclusion, all types of land-use conversion significantly improved the conditions of the topsoil, but conversion from cropland to shrubland II, forested land, and grassland, especially shrubland II and grassland, were more effective for improving soil conditions in deeper layers.

Keywords: particle-size distribution; Grain for Green project; multifractal feature; soil erosion

1. Introduction

The Loess Plateau of China covers approximately $62.4 \times 10^4$ km$^2$ [1], and is known for its long agricultural history and serious soil erosion [1,2]. The erosion has led to massive losses of soil and water, soil degradation, and ecological deterioration [3,4]. The Chinese government launched the state-funded “Grain for Green” project in 1999, which encouraged and facilitated the conversion of croplands with slopes $>15^\circ$ to forests and grasslands to control soil erosion and restore the ecological environment [2–4]. Forested land, shrubland, and grassland are now common on the Loess Plateau.

Soil erodibility is an important factor determining the rate of soil loss and is represented by an erodibility factor ($K$). $K$ can be directly measured by the long-term monitoring of erosion in runoff plots, which is accurate but costly and time-consuming [5,6]. Techniques have been
developed to estimate $K$ from readily available data for soil properties. $K$ estimated with the Erosion-Productivity Impact Calculator (EPIC) model is of particular interest to this study and was calculated using soil organic-carbon content and particle-size distribution (PSD) [7]. Zhang et al. (2008) reported that measured $K$ and the $K$ estimated from data for soil properties in China were strongly linearly correlated, although the calculated values were systematically higher than the measured values [8]. Recent extensive studies have evaluated the effectiveness of land-use conversion and have demonstrated that conversion from sloped cropland to green land greatly contributed to the improvement of soil conditions and effectively protected against erosion [9–11]. These positive effects of conversion may also have a large influence on the distribution of soil particles, because changes in soil conditions and erodibility can intimately affect fractions of fine particles [4,12].

PSD is a fundamental physical attribute of soil that greatly influences soil-moisture migration, solution transformation and soil erosion [13–15]. Characterizing its variation is therefore important for understanding and quantifying soil structure and dynamics. Multifractal analysis using laser-diffraction technology is commonly used by pedologists worldwide to characterize PSDs [16–18]. Multifractal analysis provides detailed information about the heterogeneity of a PSD [12,19], and this information can be expressed using multifractal spectra and parameters. The Rényi spectrum ($D_q$) and singularity spectrum ($f(\alpha)$) are used to characterize the scaling properties [20] and heterogeneity of PSDs [21], respectively. Multifractal parameters mainly include the capacity dimension ($D_0$), entropy dimension ($D_1$), correlation dimension ($D_2$) and Hölder exponent of order zero ($\alpha_0$), which synthetically characterize PSD systems [18,20,22] (see the Materials and Methods section for details). Many studies have successfully applied multifractal spectra and parameters for characterizing the changes of PSDs in soils of the same or different texture. Martín and Montero (2002) proposed that $f(\alpha)$ was useful for the characterization of PSDs [23]. Wang et al. (2008) reported that $D_0$ and $D_1$ were significantly influenced by land-use on the Loess Plateau [12]. Paz-Ferreiro et al. (2010) found that the multifractal analysis of PSDs could provide further insight for verifying variation between plots [17]. Multifractal analysis is therefore a potential tool of great interest for detecting modifications of soil physical properties due to changes in land management, such as type of cultivation and land-use conversion.

Many studies of the effect of land-use conversion on the Loess Plateau of China have focused mainly on the biochemical rather than the physical properties of soil [2,9,24]. Wang et al. (2008) studied the multifractal characteristics of PSD under different land-use types but mainly studied the effect of land-use and topographical factors on multifractal parameters [12]. The changes in the multifractal features and their causes have not been well studied, and few reports addressing these scientific questions are yet available, which was the motivation behind this study. We therefore analyzed soil-nutrient contents, erodibility, and the multifractal features of PSDs of five common land-use types on the Loess Plateau approximately 35 years after their conversion. The goals of this study were to: (1) assess the effect of land-use conversion on soil nutrients, erodibility, and PSDs using multifractal analysis; and (2) identify the causes of the changes in soil PSDs.

2. Materials and Methods

2.1. Study Area

This study was conducted in Ansai County (36°31′–37°20′ N and 108°52′–109°26′ E, 1010–1431 m a.s.l.) in Shaanxi Province in the central part of the Loess Plateau (Figure 1), which is well known for its high rates of erosion [25]. This area has a typical semiarid continental climate with a mean annual temperature of 8.8 °C and a mean annual precipitation of 549.1 mm, but temperature and precipitation are highly variable (74.3% of the rain falls between June and September). The landform is a typical hilly-gullied loessial landscape with deeply incised gullies. The soil is a Calcaric Regosol in the WRB reference system [26], originating from wind-blown deposits, and is characterized by a yellow color, absence of bedding, silty texture, looseness, macroporosity, and wetness-induced collapsibility [5]. These characteristics have contributed greatly to the severe soil erosion.
Substantial efforts have been made by the Chinese government since the 1950s to control soil erosion on the Loess Plateau, but the effects were not evident [2]. The state-funded “Grain for Green” project was initiated in 1999 to control soil erosion and restore the ecological environment. All croplands with slopes >15° were converted to green land [27]. The typical vegetation in the study area presently includes herbs such as *Stipa bungeana* and *Artemisia sacrorum*, shrubs such as *Caragana microphylla* and *Hippophae rhamnoides*, and woody plants such as *Robinia pseudoacacia* [25,27].

2.2. Experimental Design and Soil Sampling

The five commonest land-use types in this region were selected in September 2011: forested land, shrubland with *Caragana korshinskii* (Shrubland I), shrubland with *Hippophae rhamnoides* (Shrubland II), grassland, and abandoned sloped cropland (ASC) that had been abandoned for less than one year for comparison (Figure 2). We selected the ASC location rather than an active sloped cropland to reduce the influence of human disturbance on soil PSDs. The selected locations had been subjected to similar farming practices before the initiation of the ecological project and had been revegetated approximately 35 years ago. The forested land was revegetated mainly with *Robinia pseudoacacia*, and the grassland was mainly covered by perennial *Stipa bungeana* and *Artemisia sacrorum*. Each land-use is described in Table 1.

| Land-Use Type   | Restoration Age (Year) | Altitude (m) | Slope (°) | Main Vegetation or Crop Species               |
|-----------------|------------------------|--------------|-----------|----------------------------------------------|
| ASC             | -                      | 1270         | 19        | -                                            |
| Shrubland I     | 36                     | 1211         | 20        | *Caragana microphylla*                        |
| Shrubland II    | 35                     | 1133         | 19        | *Hippophae rhamnoides*                       |
| Forested land   | 37                     | 1237         | 30        | *Robinia pseudoacacia*                       |
| Grassland       | 35                     | 1159         | 18        | *Stipa bungeana, Artemisia sacrorum*         |

ASC: sloped cropland abandoned for <1 year.
Soil samples were collected from a total of 15 sites, three for each land-use type (Figure 1B). These sites had similar topographic characteristics (elevations and slopes), and all investigated soils had developed from the same parental materials. Soil samples were collected at each site from four randomly selected points using a soil auger (4 cm diameter). The samples were separately collected from five layers, 0–10, 10–20, 20–30, 30–50, and 50–100 cm, and the samples from the four points for the same layer were mixed to produce a composite sample for each layer and site. The mixed samples were air-dried and passed through both a 0.25 and a 1.0 mm sieve after removing the roots, stones, and debris for the determination of soil organic carbon (SOC), total nitrogen (TN), and total phosphorus (TP) contents and PSDs.

2.3. Laboratory Analysis

SOC was determined by the Walkley–Black method [28], TN by the Kjeldahl method [29], and TP by molybdenum antimony blue colorimetry [30]. Soil PSDs were analyzed by laser diffraction using a Longbench Mastersizer 2000 (Malvern Instruments, Malvern, UK). PSD was described based on the percentages of clay (<0.002 mm), fine silt (0.002–0.02 mm), coarse silt (0.02–0.05 mm), and sand (0.05–1 mm). Clay and fine silt were considered fine soil particles and coarse silt and sand were considered coarse particles.

2.4. Multifractal Theory

Multifractal analysis of particle distributions over an interval of sizes \( l \) commonly uses successive partitions of the interval in dyadic scaling down [31]. With a diameter \( l \) of interval \( I \), dyadic partitions in \( k \) stages (\( k = 1, 2, 3, \ldots \) ) generate a number of cells \( N(\varepsilon) = 2^k \) with diameter \( \varepsilon = L \times 2^{-k} \) that cover the initial interval \( I \). At every size scale \( \varepsilon \), a number \( N(\varepsilon) = 2^k \) of cells are considered, and their

Figure 2. Photographs of the land-use types. (A) Forested land with *Robinia pseudoacacia*; (B) grassland with *Stipa bungeana* and *Artemisia sacrorum*; (C) shrubland I with *Caragana microphylla*; (D) shrubland II with *Hippophae rhamnoides*; and (E) sloped cropland abandoned for <1 year.
which are termed the capacity, entropy, and correlation dimensions, respectively [18,20].

\[ \mu \]

where \( q \) is concentrated. Finally, the measure itself is replicated when \( q \) is highly concentrated are amplified, and \( q \) provides a tool for inspecting the denser and rarer regions of \( \mu \). When \( q >> 1 \), regions where \( \mu \) is highly concentrated are amplified, and \( q << -1 \) indicates the amplification of regions where \( \mu \) is less concentrated. Finally, the measure itself is replicated when \( q = 1 \).

2.5. Erodibility (K)

\( K \) is calculated using SOC content and soil PSD in the EPIC model [7] as:

\[ K = \{0.2 + 0.3 \exp[-0.0256\text{SAN}(1 - 0.01\text{SIL})]\} \times [\text{SIL}/(\text{CLA} + \text{SIL})]^{0.3} \times \{1.0 - 0.25C/[C + \exp(3.72 - 2.95C)]\} \times \{1.0 - 0.7\text{SNI}/[\text{SNI} + \exp(-5.51 + 22.9\text{SNI})]\} \]
where SAN, SIL, and CLA are the sand (%), silt (%), and clay (%) fractions, respectively. C is the SOC content (%), and SNI = 1 – SAN/100.

2.6. Statistical Analysis

The data in the figures and tables are means for each sample. All statistical analyses were implemented using various packages within the R statistical computing environment (R version 3.2.3). One-way analyses of variation compared the effects of land-use type and soil depth on the soil nutrients, texture, and multifractal parameters. Duncan’s tests separated the means of these variables at \( p < 0.05 \).

Network analyses were used to show the composition of, and interactions between, multiple elements in the communities. A matrix of the correlations between all trait pairs was generated by network analysis based on significance levels at \( p < 0.05 \) or on both the significant level and correlation coefficients of \( r > 0.4 \). These pairs were considered as a network in which a vertex corresponds to a trait, and a link between two vertices corresponds to significant correlations between these two traits. This network was then plotted based on the adjacency matrix using the R igraph package.

3. Results

3.1. Effects of Land-Use Type and Soil Depth on Soil Nutrient Content and Texture

SOC, TN, clay, and fine-silt contents in the 0–10 cm layer (topsoil) were significantly higher and the coarse-silt content and erodibility were significantly lower in all older land-use types compared to ASC. In the 10–30 cm layers (shallow soil), SOC and TN contents in shrubland II and grassland, clay content in all older land-use types, and fine-silt content in shrubland II, forested land, and grassland were significantly higher, whereas coarse-silt content and erodibility in all older land-use types were significantly lower, relative to ASC. In the 30–100 cm layers (deep soil), SOC, clay, and fine-silt contents in shrubland II and grassland were significantly higher and sand content in grassland was significantly lower than in ASC (Table 2).

SOC and TN contents generally tended to decrease with soil depth and remained unchanged below 30 cm. TP content was highest in shrubland I and forested land. Changes of soil texture with soil depth were not obvious but were observed in several of the land-use types.

Table 2. Effects of land-use type and soil depth on soil nutrients (g kg\(^{-1}\)) and soil texture (%).

| Soil Property | Soil Layer (cm) | ASC | Shrubland I | Shrubland II | Forested Land | Grassland |
|---------------|----------------|-----|-------------|--------------|---------------|-----------|
| SOC           | 0–10           | 3.652 Ac | 6.819 Ab     | 13.17 Aa     | 8.454 Ab      | 7.37 Ab   |
|               | 10–20          | 3.263 Abc | 3.871 Bc     | 7.844 Ba     | 4.477 Bbc     | 5.655 Bb  |
|               | 20–30          | 2.493 Bcc | 3.084 BCbc   | 6.52 BCa     | 3.314 Bbc     | 4.173 Bcb |
|               | 30–50          | 2.123 Cbc | 2.186 Cbc    | 5.497 CDa    | 1.847 Cc      | 3.359 Cb  |
|               | 50–100         | 1.744 Cc  | 1.793 Cc     | 4.234 Da     | 1.647 Cc      | 2.935 Cb  |
| TN            | 0–10           | 0.468 Ad  | 0.734 Ac     | 1.287 Aa     | 0.886 Ab      | 0.8 Abc   |
|               | 10–20          | 0.375 Bc  | 0.472 Bbc    | 0.788 Bb     | 0.552 Bb      | 0.626 Bb  |
|               | 20–30          | 0.269 BCc | 0.374 BCbc   | 0.646 BCa    | 0.457 Bb      | 0.453Cb   |
|               | 30–50          | 0.298 Cb  | 0.272 CDbc   | 0.538 Ca     | 0.317 Cb      | 0.35 Cb   |
|               | 50–100         | 0.249 Cab  | 0.227 Db     | 0.357 Da     | 0.276 Cab     | 0.299 Cab |
| TP            | 0–10           | 0.586     | 0.596 A      | 0.543        | 0.571 A       | 0.546     |
|               | 10–20          | 0.579     | 0.546 B      | 0.601        | 0.559 AB      | 0.578     |
|               | 20–30          | 0.564     | 0.545 B      | 0.569        | 0.537 AB      | 0.563     |
|               | 30–50          | 0.553     | 0.532 B      | 0.574        | 0.522 B       | 0.562     |
|               | 50–100         | 0.555     | 0.543 B      | 0.552        | 0.533 AB      | 0.539     |
| Clay          | 0–10           | 4.133 c    | 5.46 b       | 6.965 a      | 4.956 Ab      | 5.431 ab   |
|               | 10–20          | 3.898 c    | 5.819 b      | 7.678 a      | 5.441 Ab      | 5.731 b    |
|               | 20–30          | 3.754 c    | 5.545 b      | 7.468 a      | 5.206 Ab      | 6.29 ab    |
|               | 30–50          | 3.905 c    | 5.501 bc     | 7.602 a      | 5.366 Abc     | 6.14 ab    |
|               | 50–100         | 3.886 c    | 5.478 b      | 7.065 a      | 3.886 Bc      | 6.386 ab   |
Multifractal Characterization of Soil PSDs

The erodibility in the 0–10 cm layer of all older land-use types and in the 10–100 cm layers of shrubland II and grassland were significantly lower than in ASC (Figure 3). Erodibility generally tended to increase with soil depth and remained unchanged below 20 cm.

![Figure 3](Image)

**Figure 3.** Effect of land-use conversion and soil depth on erodibility. Numerical values are means ± standard deviation for three samples. Different uppercase letters indicate significant differences between treatments at each depth, and different lowercase letters within a column indicate significant differences between depths within each treatment, and different lowercase letters within a row indicate significant differences between treatments at each depth (Duncan’s test, p < 0.05). ASC: sloped cropland abandoned for <1 year.

### 3.2. Effects of Land-Use Type and Soil Depth on Soil Erodibility

The erodibility in the 0–10 cm layer of all older land-use types and in the 10–100 cm layers of shrubland II and grassland were significantly lower than in ASC (Figure 3). Erodibility generally tended to increase with soil depth and remained unchanged below 20 cm.

### 3.3. Multifractal Characterization of Soil PSDs

Selected examples of Rényi spectra ($D_q$) are shown in Figure 4. These curves were calculated for 0.2 $q$ steps in the range of moments from −10 to 10. The $D_q$ spectra were typical sigmoidal curves, notably decreased as $q$ increased, and differed in shape among land-use types in both the 0–10 and 10–20 cm layers.
Figure 4. Rényi spectra ($D_q$) of randomly selected samples in each soil layer of the various land-uses.

Singularity spectra, $f(\alpha)$, of selected samples are shown in Figure 5. The shapes of the $f(\alpha)$ spectra of the selected samples varied greatly among the land-use types for the same soil layers, especially the 0–10 and 10–20 cm layers, even though the spectra were characterized by a typical concave downward shape. All $f(\alpha)$ spectra had long left components, but the right components were quite different.

Figure 5. Singularity spectra ($f(\alpha)$) of randomly selected samples in each soil layer of the various land-uses.

3.4. Effects of Land-Use Type and Soil Depth on the Multifractal Parameters

$D_0$ in the 0–20 cm layers were significantly higher for shrubland I and grassland than the other land-use types. $D_0$ did not differ significantly among the land-use types in the 20–100 cm layers. $D_1$ in the 0–20 cm layers in all the older land-use types (i.e., not ASC); in the 20–50 cm layers of shrubland II, forested land, and grassland; and in the 50–100 cm layer of shrubland II were significantly higher than in ASC. $D_2$ was significantly higher in the 0–10 cm layers of all the older land-use types and in the 10–50 cm layers of shrubland II, forested land, and grassland than ASC. $\alpha_0$ was significantly higher in the 0–10 cm layers of shrubland I and grassland than ASC (Table 3).
In shrubland I and grassland, $D_0$, $D_1$, $D_2$, and $\alpha_0$ were significantly higher and $D_1/D_0$ was significantly lower in the 0–10 cm layer than the other layers. The multifractal parameters in the other three land-use types differed by minor significance with increasing depth (Table 3).

### Table 3. Effects of land-use type and soil depth on the multifractal parameters.

| Parameter | Soil Layer (cm) | ASC          | Shrubland I | Shrubland II | Forested Land | Grassland |
|-----------|----------------|--------------|-------------|--------------|---------------|-----------|
|           | 0–10           | 0.874 b      | 0.948 Aa    | 0.889 Ab     | 0.887 b       | 0.927 Aa  |
|           | 10–20          | 0.871 b      | 0.885 Ba    | 0.877 Bab    | 0.871 b       | 0.884 Ba  |
|           | 20–30          | 0.873        | 0.88 B      | 0.876 B      | 0.88          | 0.878 B   |
|           | 30–50          | 0.871        | 0.88 B      | 0.877 B      | 0.876         | 0.874 B   |
|           | 50–100         | 0.871        | 0.879 B     | 0.876 B      | 0.871         | 0.871 B   |
| $D_1$     | 0–10           | 0.846 c      | 0.876 Aa    | 0.862 b      | 0.857 Ab      | 0.866 Aab  |
|           | 10–20          | 0.842 c      | 0.848 Bb    | 0.858 a      | 0.855 Aa      | 0.857 Ba  |
|           | 20–30          | 0.842 b      | 0.847 Bb    | 0.856 a      | 0.857 Aa      | 0.857 Ba  |
|           | 30–50          | 0.842 b      | 0.846 Bab   | 0.858 a      | 0.856 Aa      | 0.856 Ba  |
|           | 50–100         | 0.843 b      | 0.848 Bab   | 0.856 a      | 0.843 Bb      | 0.855 Bab  |
| $D_1/D_0$ | 0–10           | 0.968 a      | 0.924 Bb    | 0.970 a      | 0.967 a       | 0.935 Bb  |
|           | 10–20          | 0.966 ab     | 0.959 Ab    | 0.978 a      | 0.962 a       | 0.970 Aab |
|           | 20–30          | 0.964 ab     | 0.962 Ab    | 0.978 a      | 0.973 ab      | 0.976 Aab |
|           | 30–50          | 0.966 ab     | 0.961 Ab    | 0.978 a      | 0.977 a       | 0.979 Aa  |
|           | 50–100         | 0.968 ab     | 0.965 Ab    | 0.977 ab     | 0.968 Ab      | 0.982 Aa  |
| $D_2$     | 0–10           | 0.829 b      | 0.845 Aa    | 0.848 a      | 0.845 Aa      | 0.845 a   |
|           | 10–20          | 0.822 b      | 0.828 Bb    | 0.841 a      | 0.844 Aa      | 0.842 a   |
|           | 20–30          | 0.823 b      | 0.827 Bb    | 0.839 a      | 0.844 Aa      | 0.843 a   |
|           | 30–50          | 0.823 b      | 0.826 Bb    | 0.84 ab      | 0.844 Aa      | 0.841 ab  |
|           | 50–100         | 0.825        | 0.828 B     | 0.839        | 0.825 B       | 0.839     |
| $\alpha_0$| 0–10           | 0.945 c      | 1.073 Aa    | 0.963 Ac     | 0.984 bc      | 1.059 Aab |
|           | 10–20          | 0.942        | 0.963 B     | 0.932 B      | 0.929         | 0.966 B   |
|           | 20–30          | 0.95         | 0.955 B     | 0.928 B      | 0.959         | 0.949 B   |
|           | 30–50          | 0.941        | 0.954 B     | 0.927 B      | 0.946         | 0.932 B   |
|           | 50–100         | 0.941 ab     | 0.949 Ba    | 0.929 Bab    | 0.941 ab      | 0.92 Bb   |

Numerical values are means ± standard deviation for three samples. Different uppercase letters within a column indicate significant differences between depths within each treatment, and different lowercase letters within a row indicate significant differences between treatments at each depth (Duncan’s test, $p < 0.05$). ASC: sloped cropland abandoned for <1 year.

3.5. Relationships between the Multifractal Parameters and Selected Soil Properties and Erodibility

The correlation network including the traits of soil nutrients, texture, erodibility, and multifractal parameters were plotted to test the relationships among these parameters. All significant correlations ($p < 0.05$) were visualized as edges in the network (Figure 6A), and the network was simplified based on the correlation coefficients and statistical significance (Figure 6B, $r > 0.4$ and $p < 0.05$). The size of a vertex in the network was dependent on the node degree: the larger the node degree of one vertex, the stronger the connection with other vertices, indicating a more important corresponding trait in the network. The vertices for clay, fine-silt, coarse-silt, sand, SOC, and TN contents and for $D_0$, $D_1$, $D_2$, and erodibility were obviously larger than those for the other parameters. Considering the importance of multifractal parameters and their relationships with other soil properties, $D_1$ and $D_2$ were selected for the analyses of linear regression to quantify the relationships. $D_1$ and $D_2$ were linearly correlated positively with SOC and TN contents but negatively with erodibility ($p < 0.001$) (Figure 7). $D_1$ and $D_2$ were correlated positively with clay and fine-silt contents, but correlated negatively with coarse-silt and sand contents ($p < 0.001$) (Figure 8). The slope coefficients of the regression lines were highest for the models between erodibility and $D_1$ and $D_2$ ($-0.283$ and $-0.294$, respectively), and the slope coefficients of the regression lines were higher for the models between clay content and $D_1$ and $D_2$ (0.004 and 0.005, respectively) than for the other particle-size classes.
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Figure 6. Network plot showing the associations between the multifractal parameters and selected soil properties and erodibility. (A) Significant correlations ($p < 0.05$); and (B) moderately or highly significant correlations ($r > 0.4$, $p < 0.05$).

![Network plot showing the associations between the multifractal parameters and selected soil properties and erodibility.](image)

Figure 7. Relationships between multifractal parameters and SOC and TN contents and erodibility. *** Significant at $p < 0.001$.

![Relationships between multifractal parameters and SOC and TN contents and erodibility.](image)

Figure 8. Relationships between multifractal parameters and soil texture. *** Significant at $p < 0.001$.

![Relationships between multifractal parameters and soil texture.](image)
4. Discussion

4.1. Land-Use Conversion Affects Soil Nutrients, Texture, and Erodibility

Land-use conversion from cropland to other land-use types can improve soil properties and decrease soil erosion, but with different effects. This finding was consistent with previous studies showing that conversion from sloped cropland to perennial vegetation could greatly improve soil nutrients [11] and SOC sequestration [25,35] and decrease the erosion of topsoil [9,36]. Our results also supported these observations, showing that all older land-use types had significantly higher SOC, TN, and fine-soil contents and lower topsoil erodibility. Soil-nutrient contents did not improve in shrubland I and forested land in the shallow soil layers, and SOC and fine-particle contents increased significantly while erodibility decreased significantly in shrubland II and grassland in deep soil layers. These changes were mainly due to the high degree of vegetation coverage and the high input of residues [2,24,37]. Stable ecosystems and new microclimatic regimes can be established after conversion in about 35 years [38], with well-developed root systems, dense canopies for forests and shrubland, and better vegetation coverage for grassland, with high amounts of ground litter. These traits can potentially improve soil conditions, decrease erosion of the topsoil by reducing raindrop splash and impeding surface runoff, which can consequently protect fine soil particles [13,39]. Soil nutrients did not significantly increase in shallow layers in shrubland I and forested land, likely because soil organic matter in these two land-use types is more easily oxidized or degraded by microorganisms under the specific microclimates. Sun et al. (2016) found relatively higher amounts of labile carbon in shrubland with *Caragana microphylla* [25]. SOC and fine-particle contents were significantly higher in the deep soil layers in shrubland II and grassland, indicating that these two land-use types facilitated the sequestration of soil carbon and improved the structure of deep soil.

SOC and TN contents decreased significantly and erodibility increased significantly with depth, but changes of soil texture were not obvious. Previous studies in the same region reported similar results, showing that SOC and TN contents were significantly higher in the surface soil than in deeper layers [1,25,27]. The higher SOC and TN contents and lower erodibility were mainly attributed to the improvement of soil quality and structure. Residues such as litter and roots were more abundant and humic processes were more efficient in surface soil relative to deep soil, which facilitated the increase of soil nutrients and amelioration of soil physical properties. In contrast, relatively few residues are imported to deep soil, where many nutrients are absorbed by root systems to meet the needs for photosynthesis [2,37]. PSD is an essential physical attribute of a soil and is more stable compared to chemical properties, and textural classes can exhibit a wide range of PSDs [12,17], so associating changes of soil texture with soil depth is difficult.

4.2. Land-Use Conversion Affects the Multifractal Features of Soil PSDs

The Rényi spectra ($D_q$) and singularity spectra ($f(\alpha)$) were able to characterize the PSDs well and sensitively identified the differences in PSDs among the land-use types. The $D_q$ spectra were typical sigmoidal curves and notably decreased as $q$ increased, indicating that PSDs in the various land-use types presented multifractal rather than monofractal behavior. The different curves among the land-use types in the 0–10 and 10–20 cm layers suggested diverse scaling properties of these PSDs. The different shapes of the $f(\alpha)$ spectra suggested different heterogeneities of soil PSDs among the land-use types for the same soil layers, especially the 0–10 and 10–20 cm layers. The $D_q$ and $f(\alpha)$ spectra of the PSDs in the 0–20 cm layers changed significantly after 35 years of land-use conversion, indicating that land-use was an important factor in the distribution of soil particles, and these changes were determined well by the multifractal modes. The multifractal features of PSDs change mainly due to improvements of soil quality [2,25,37] and the reduction of erosion [9,36] of the surface soil, which generally facilitate the improvement of soil structure and increase the proportions of microaggregates and fine particles [40–42] and accordingly change the multifractal features of soil PSDs.
Land-use conversion had a positive effect on the increase of the multifractal parameters such as $D_0$, $D_1$, $D_2$, and $\alpha_0$, but $D_1/D_0$ changed little. $D_0$ and $\alpha_0$ in shrubland I and grassland and $D_1$ and $D_2$ in all the other land-use types were significantly higher in the topsoil. $D_1$ and $D_2$ in the 10–50 cm layers of shrubland II, forested land, and grassland and $D_1$ in the 50–100 cm layers of shrubland II were significantly higher than in ASC. As previously stated, different multifractal parameters represent different information for soil PSDs. High values of these multifractal parameters indicate that PSDs have wide ranges, high heterogeneities, and are more homogeneous among all intervals [21,43,44]. Increases in multifractal parameters may be attributed to increases in fine-soil particles [40,45,46]. The increase in fine-soil particles in the topsoil was likely due to the comprehensive effect of greatly improved soil quality and reduced soil erosion after the rehabilitation of the vegetation [10,38,47].

A high degree of vegetation coverage was attained 35 years after the land-use conversion, which could reduce soil erosion by reducing rain splash and could also improve the amount of soil organic matter and structure by increasing aboveground and root biomasses. High concentrations of soil organic matter and low soil erosion generally facilitate the improvement of soil structure and increase microaggregates and fine particles [5,13,39,48]. The penetration and fixation of developed root systems in shrublands, forested land, and grassland could also protect fine particles from erosion, thereby preserving the fine particles [4,13]. Increases in fine particles in non-topsoil layers, however, are mainly due to the improvement of soil quality and the interaction of root systems. Plant roots usually exude substrates, some of which are viscous, such as polysaccharides, phenolic compounds, and polygalacturonic acid that contribute greatly to the cohesion of fine soil particles [4]. In conclusion, land-use conversion facilitated the increase of fine particles and thus potentially contributed to the wide range of soil PSDs and the greater irregularity and heterogeneity of the PSDs.

Soil depth had a significant effect on the multifractal parameters only in shrubland I and grassland. $D_0$, $D_1$, $D_2$, and $\alpha_0$ were significantly higher, but $D_1/D_0$ was significantly lower, in the 0–10 cm than the other layers, suggesting that PSDs in the topsoil of these two land-use types were more heterogeneous relative to the deep soil layers. Higher multifractal parameters in the topsoil (0–10 cm) can be due to a higher content of fine particles [40]. The highest SOC content and lowest erodibility in the topsoil of these two land-use types may have greatly contributed to the higher content of fine particles relative to deep soil. Surface weathering can also contribute to an increase in fine particles [48]. The lower $D_1/D_0$ in the topsoil of shrubland I and grassland may have been largely due to the higher value of the denominator ($D_0$).

4.3. Multifractal Parameters Were Associated with the Selected Soil Properties and Erodibility

The network analysis clearly indicated that soil nutrients, texture, erodibility, and the multifractal parameters were significantly correlated with each other ($p < 0.05$) and that the node degrees for clay, fine-silt, coarse-silt, sand, SOC, and TN contents and $D_1$, $D_2$, and erodibility were larger than those for the other traits, indicating that these selected traits were more connected with the others and played more important roles in the network. The network could clearly identify the interrelationships but not the quantitative relationships between the multifractal parameters and the other soil properties. We eliminated $D_0$, $D_1/D_0$, and $\alpha_0$ from the analyses of linear regression to simplify and better analyze these quantitative relationships. $D_1$ and $D_2$ were linearly and correlated positively with SOC, TN, clay, and fine-silt contents but negatively with erodibility and coarse-silt and sand contents ($p < 0.001$). This result suggested that $D_1$ and $D_2$ can be used as indicators of the changes in soil quality and erosion after land-use conversion, because SOC and TN contents are important indices for the assessment of soil quality and structural stability [48,49] and because erodibility calculated based on the EPIC model can estimate soil erosion well for the Loess Plateau [5,50]. Additionally, the effect of erodibility was largest on $D_1$ and $D_2$, and the effect of clay content on $D_1$ and $D_2$ was larger than for silt and sand contents, based on the slope coefficients of the models of linear regression. These results indicated that erodibility was the vital factor influencing multifractal characterization, so the effect of land-use conversion on the multifractal features of PSDs may mainly be due to a decrease in soil erosion, which
would increase the clay content and the heterogeneity of the PDSs, thereby changing the multifractal features of the PDSs.

5. Conclusions

The Rényi spectra \((D_q)\) and singularity spectra \((f(\alpha))\) characterized the PDSs well and sensitively represented the changes of PDSs after land-use conversion. Land-use conversion greatly affected soil nutrients, erodibility, and the multifractal parameters. Specifically, all types of land-use conversion significantly improved the properties of the topsoil (0–10 cm), but the effect of shrubland I and even forested land decreased with depth. All types of land-use conversion significantly increased \(D_1\) and \(D_2\) in the topsoil, and \(D_1\) and \(D_2\) in the 10–50 cm layers of shrubland II, forested land, and grassland and \(D_1\) in the 50–100 cm layers of shrubland II were significantly higher relative to ASC. The other multifractal parameters also varied after land-use conversion but showed no clear trend. \(D_1\) and \(D_2\) were sensitive to the dynamics of soil nutrients and fine particles and could act as potential indices for quantifying changes in soil properties and erosion. Multifractal theory was therefore a useful tool for characterizing PDSs on the Loess Plateau of China. All types of land-use conversion significantly improved topsoil conditions, but conversion from cropland to shrubland II, forested land, and grassland, especially shrubland II and grassland, were more effective for improving the conditions in deeper soil layers.

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