The role of spin–orbit effects in the mobility of N\textsuperscript{+} ions moving in a helium gas at low temperature\textsuperscript{*,**}

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Received 5 March 2020 / Received in final form 3 June 2020
Published online 23 July 2020
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Abstract. The mobility of N\textsuperscript{+} ions in ground-state helium gas at very low temperature is examined with explicit inclusion of spin–orbit coupling effects. The ionic kinetics is treated theoretically with the three-temperature model. The N\textsuperscript{+}–He interaction potentials, including spin–orbit coupling, are determined using high-level ab initio calculations. Then, the classical and quantal transport cross sections, both needed in the computation of the mobility coefficients, are calculated in terms of the collisional energy of the N\textsuperscript{+}–He system. The numerical results, at temperature 4.3 K, show the spin–orbit interactions have negligible effect on the mobility coefficients.

1 Introduction

Ion mobility experiments in cooled buffer gases have long been of interest [1]. They are particularly relevant in analytical chemistry, because various large ions can have quite different ion mobilities even if they have the same molar masses. The variations of mobility over wide ranges of gas temperature $T$ and/or electric field strength $E$ serve as excellent probes of the forces between the ions and the atoms or molecules of the gas through which they move. In addition, the mobility data are also needed in laboratory studies of the kinetics of ion-molecule reactions and in applications to the earth’s ionosphere [2]. There have been many advances in the kinetic theory of ion mobility, such as the three-temperature (3T) theory [1], and they have now reached the point where the mobility of atomic ions in cooled buffer gases can be calculated with ab-initio methods of higher accuracy than can be measured [3].

By making use of the Gram–Charlier approach [4] and quantum-mechanical transport cross sections, we have computed in a previous paper the C\textsuperscript{+} ionic mobility in He gas at the two specific temperatures 4.3 and 77 K [5].

The same mobility has also been examined classically by Tuttle et al. [6] with the inclusion of the spin–orbit (SO) couplings. Both theoretical works have been unable to reproduce the shallow minimum of the mobility coefficient at 4.3 K as measured by Matoba et al. [7]. Such failures incited us to apply both quantal and classical methods to a different system, namely, the open-shell ionic NH\textsuperscript{e+} diatom, at $T = 4.3$ K. We use three-temperature theory and the obtain the quantal transport cross sections with the inclusion of the spin–orbit effects to explore theoretically the causes of the unusual behaviour and peculiar shape of the N\textsuperscript{+} ion mobility in a cooled buffer gas made exclusively of ground helium at the very low temperature 4.3 K. The results are compared with the measurements of Sanderson et al. [8] obtained with a cooled selected ion drift tube at the temperature 4.35 K. The low-temperature variation of the ion mobility with electric field is found to be particularly sensitive to the various approximations made in its evaluation. We have therefore chosen to compute the ab initio NH\textsuperscript{e+} potential-energy curves, including the effects of spin–orbit (SO) couplings, to a controlled high accuracy, as well as investigating the possible effects of using the full quantum-mechanical approximations to the dynamics instead of a classical treatment.

In the following sections, we report the details of the present calculations of the N\textsuperscript{+}–He interaction potentials that arise from the lowest atomic asymptotes of the open-shell N\textsuperscript{+} (\textsuperscript{1}P\textsubscript{1}) + He (\textsuperscript{1}S\textsubscript{0}) system, the quantal and classical transport cross sections, and the mobility variations with electric strength, as implemented in the Fortran codes PC.F90 and GC.F90 of Viehland [9].

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\textsuperscript{*} Electronic Supplementary Information (ESI) available: All the data points derived from the ab initio potentials of the ground N\textsuperscript{+}–He molecular states, without and with the spin–orbit (SO) effects.

\textsuperscript{**} Supplementary material in the form of one pdf file available from the Journal web page at https://doi.org/10.1140/epjd/e2020-10138-0.
Unless otherwise specified, atomic units (a.u.) are used throughout this paper; in particular, energies are given in hartrees ($E_h$), distances in bohrs ($a_0$), and $\hbar = 1$.

2 N$^+$–He interaction potentials

In this section, we describe the ab initio method employed in the generation of the potential-energy curves of the diatomic system correlated with the ground N$^+$ ($2s^22p^2; 3P$) state that interacts with the ground He ($1s^2; 1S$) including the effects of the spin–orbit interactions.

The inclusion of the SO interactions produces three levels from the splitting of the N$^+$ ($3P$) state: the lowest state is $3P_0$, the middle state $3P_1$ is higher by 48.74 cm$^{-1}$ and the upper state $3P_2$ is 130.78 cm$^{-1}$ higher [10]. Consequently, the SO interactions lead to the separation of the $3\Sigma^+_0$ state into the $3\Pi_0$ and $3\Sigma^+_1$ levels, and the $3\Pi$ state splits into the three distinct levels, namely $3\Pi_0$, $3\Pi_1$, and $3\Pi_2$.

In order to determine the interaction potentials for all the relativistic diatomic states, we first performed non-relativistic calculations for internuclear distances in the range $1.0 \leq R \leq 40.6$ using the spin-restricted open-shell variant of the couple-cluster method with single and double excitations and perturbative treatment of connected triple excitations (RCCSD(T)) [11, 12]. In order to accurately represent weak long-range interactions dominated by polarisation effects, we used the doubly-augmented correlation-consistent basis sets [13,14], extrapolating the quadruple- (d-aug-cc-VQZ) and quintuple- (d-aug-cc-V5Z) set correlation energies using the $x^{-3}$ model [15], and applying the standard counterpoise correction for basis-set superposition error [16]. Spin–orbit coupling was then introduced by computing an interaction Hamiltonian using the Breit–Pauli spin–orbit operator and the internally-contracted multireference configuration interaction (MRCI) method [17,18]. All calculations were carried out using the MOLPRO package [19].

The generated data points of the non-SO and SO interaction potentials are displayed in Figures 1a and 1b, respectively and some of their data points are listed in Table 1. All the data points derived from the ab initio potentials of the ground N$^+$–He molecular states, without and with the spin–orbit (SO) effects, are given in a supplementary material. In particular, the inset in Figure 1b shows the $3P_0$–$3P_2$ and $3P_0$–$3P_1$ splittings of 123.25 cm$^{-1}$ and 41.08 cm$^{-1}$, respectively, which are comparable to the experimental values of 130.77 cm$^{-1}$ and 48.74 cm$^{-1}$ [10]. Figure 1b shows that the lowest $3\Sigma^+_0$ level correlates to N$^+$ ($3P_0$) + He ($1S_0$) asymptote, the $3\Sigma^+_1$ and $3\Pi_0$–levels both correlate to N$^+$ ($3P_1$) + He ($1S_0$) asymptote, and the three highest $3\Pi_0$, $3\Pi_1$, and $3\Pi_2$ levels correlate to N$^+$ ($3P_1$) + He ($1S_0$) asymptote. It should be noted that $\Omega = +0$ for the $3\Pi_0$–level differs from $\Omega = +0$ for the $3\Pi_0$ level as obtained in the potentials calculations of Soldan et al. [20].

In using the generated NHe$^+$ potentials to compute quantum-mechanically the transport cross sections, without or with the SO effects, we slightly altered the data points in order to connect them smoothly with the Born–Mayer and the long-range forms. Indeed, in the short-range region, i.e., $R < 1.0$, the ion-atom curves follow the Born–Mayer relationship [21]

$$V_{SR} (R) = \alpha \exp (-\beta R),$$

with $\alpha$ and $\beta$ being two constant parameters. Their values are listed in Table 2. For the long-range region, namely $R > 40.6$, the extension is chosen of the analytic form [22,23]

$$V_{LR} (R) = -\frac{C_4}{R^4} - \frac{C_6}{R^6} - \frac{C_8}{R^8},$$

where $C_4$ is the dipole–dipole induction coefficient equal to half of the dipole polarizability $\alpha_4$ of the neutral helium atom, and $C_6$ and $C_8$ contain contributions from both dispersion and induction. With the basis-set described above, the CI dipole polarizability of He is 1.382; for representing

![Fig. 1. Interaction potential-energy curves of the ground N$^+$ ($3P$) He state. The dashed lines show the non-SO potentials in (a) while the solid lines show the SO potentials in (b).](image-url)
the long-range potentials, we used $\alpha_d = 1.384$ [24], with $C_6$ and $C_4$ determined as fitting parameters.

For the classical calculations, the Viehland pc.f90 code shifts only the long-range potential at the last data point $R = 40.6$ that agrees with the inverse fourth power term $R^{-4}$ to determine the $C_4$ coefficients. This accounts for the attraction between the charge on the ion and the dipole induced in the polarized neutral atom. Moreover, at a low gas temperature and for a weak electric field, the mobility is dominated by the leading term that appears in the long-range polarization energy shown in equation (2) and approaches the polarizability limit as the effective temperature tends to zero Kelvin. This mobility limit is expressed at the standard gas density by [1]

$$K_{pol} = \frac{13.853 \text{ cm}^2 \text{ V}^{-1} \text{ s}^{-1}}{\sqrt{(\alpha_d/4\pi\varepsilon_0)} / \AA^3 \mu/\text{Da}} \quad (3)$$

with $\mu$ being the reduced mass of the ion-neutral species.

In order to characterize quantitatively the present constructed potentials, we list in Table 3 the internuclear separations $\sigma$ for which $V(\sigma) = 0$, as well as the the equilibrium internuclear distance $R_e$ and the potential depth $D_e$ for each diatomic state. The $R_e$ and $D_e$ data sets are both compared with those obtained by Soldán et al. [20]. They derived these two parameters from RCCSD(T) for non-SO potentials and from unmirrored spin-free potential-energy curves for the SO potentials. The same parameters are also compared with those derived by Buentker et al. [25] from MRD-CI for the SO potentials and by Gu et al. [26] from MRD-CI and Frenking et al. [27] for the non-SO potentials. One may notice that the present determined $R_e$ and $D_e$ values are mostly in good agreement with those of Soldán et al. [20].

3 Diffusion cross sections

The diffusion or momentum-transfer cross sections $Q_d$ are the key intermediates between the ion-atom interaction potential and the diffusion or mobility coefficient. The numerical determination of $Q_d(\varepsilon)$ is usually accomplished over wide ranges of the energy $\varepsilon$ of the $N^+--$He relative motion. The collisions are supposed as occurring between two structureless species with the orbital angular momentum quantum numbers $l \geq 0$. In the case of ion-atom elastic collisions, the general expression of $Q_d(\varepsilon)$ is given by the integral [1,28]

$$Q_d(\varepsilon) = 2\pi \int_0^\pi \left(1 - \cos \theta\right) \sigma(\theta, \varepsilon) \sin \theta \, d\theta,$$

(4)
where $\sigma(\theta, \varepsilon)$ is the differential cross section for elastic scattering through the angle $\theta$ by the ion-atom interaction potential. The $\sigma(\theta, \varepsilon)$ is therefore a tool to determine the quantal and classical momentum-transfer cross sections.

### 3.1 Quantal cross sections

For the quantal calculation of the diffusion cross sections, equation (4) leads to the relationship [28]

$$Q_d(\kappa) = \frac{4\pi}{\kappa^2} \sum_{l=0}^{\infty} (l+1) \sin^2(\eta_{l+1} - \eta_l),$$  \hspace{1cm} (5)

where $\kappa = \sqrt{2\mu \varepsilon}$ is the wave number of the relative motion at energy $\varepsilon$ and $\eta_l$ are the energy-dependent phase shifts. Numerically, the quantal calculations of the phase shifts $\eta_l$ are performed up to a certain large value of the orbital angular momentum $l^*$ beyond which they are achieved with the semi-classical approximation [28,29]

$$\eta_l \approx -\mu \int_{R_0}^{\infty} \frac{V(R)}{\sqrt{(\kappa R)^2 - (l + 1/2)^2}} R dR,$$  \hspace{1cm} (6)

where the lower limit $R_0$ verifies the relationship

$$\kappa R_0 = \left(l + \frac{1}{2}\right).$$  \hspace{1cm} (7)

Equation (5) shows the orbiting resonances when the relative energy $\varepsilon$ corresponds to a significant increase in the phase shifts $\eta_l$.

In Figure 2a, we display the quantal diffusion cross sections corresponding to the non-SO NHe$^+$ states, $^3\Sigma^-$ and $^3\Pi$, and to the SO NHe$^+$ states, $^3\Sigma^+$, $^3\Pi^-$, $^3\Pi_0^-$, $^3\Pi_0^+$, $^3\Pi_1$, and $^3\Pi_2$. It clearly shows that the quantal effects are important at lower energies for the quantum-mechanical cross sections where they exhibit undulations with some regular peaks occurring at the orbiting resonances. One may observe that these orbiting resonances of the diffusion cross sections are strictly related to the energy depth of the interaction potentials and they decrease beyond it.

### 3.2 Classical cross sections

The classical diffusion cross sections are calculated, in this work, by using the Fortran code PC.F90 of Viehland [30]. The general formula of the classical momentum-transfer cross sections is given as [1]

$$Q_d(\varepsilon) = 2\pi \int_0^{\infty} [1 - \cos(\theta(b, \varepsilon))] b db,$$  \hspace{1cm} (8)

with $b$ being the impact parameter. The angle of deflection $\theta$ is defined by

$$\theta(b, \varepsilon) = \pi - 2b \int_{R_0}^{\infty} \left[1 - \frac{b^2}{R^2} - \frac{V(R)}{\varepsilon}\right]^{-1/2} \frac{dR}{R},$$  \hspace{1cm} (9)

where the distance of closest approach $R_0$ is the outermost of

$$1 - \frac{b^2}{R^2} - \frac{V(R_0)}{\varepsilon} = 0.$$  \hspace{1cm} (10)

The results of the classical momentum-transfer cross sections for the non-SO and SO NHe$^+$ states are both plotted in Figure 2b.

### 3.3 Average cross sections

Since the actual ionic state populations are not definitely known, one need to compute the average diffusion cross sections. These are generally given by the statistically weighted formula [7]

$$\overline{Q}_d = \sum_j g_j Q_d^j,$$  \hspace{1cm} (11)

where $g_j$ is the multiplicity of the considered molecular state $j$ and $Q_d^j$ is the corresponding diffusion cross section.

Hence, the average cross sections $\overline{Q}_d$ for the triplet non-SO states $^3\Sigma^-$ and $^3\Pi$ are given by the weighted sum [1]

$$\overline{Q}_d = \frac{1}{3}Q_d^\Sigma + \frac{2}{3}Q_d^\Pi.$$  \hspace{1cm} (12)
In the relativistic case, the average cross section $Q_d$ for the triplet-SO $N^+ (3P_J)$-He state is calculated from a $(1 : 3 : 5)$ mix of the cross-sections for the $3P_0$, $3P_1$, and $3P_2$ levels respectively; however these are further broken down as $3P_1$ contributions coming from a $(2 : 1)$ mix of those from the $3\Sigma_1$ and $3\Pi_0^-$ levels, and $3P_2$ from a $(1 : 2 : 2)$ mix of $3\Pi_0^+$, $3\Pi_1$, and $3\Pi_2$ levels. To show the difference between the two calculation methods, we compare in Figure 2c between the average quantum-mechanical and classical momentum-transfer cross sections, which reveals the absence of the orbiting resonances in the classical calculation for the energies below $10^{-3}$.

4 Mobility results and discussion

In this section, we employ the obtained results of the average quantal and classical transport cross sections to compute the corresponding reduced mobility coefficients $K_0$ of $N^+ (3P_J)$ in He as a function of the ratio $E/N$ of the electric field strength to the gas number density at temperature 4.3 K and also as a function of the effective temperature $T_{\text{eff}}$ defined as [1]:

$$\frac{3}{2} k_B T_{\text{eff}} = \frac{3}{2} k_B T + \frac{1}{2} M v_d^2,$$

(13)
where $T_{\text{eff}}$ characterizes the kinetic energy of an ion-neutral gas collision in the centre-of-mass frame, $M$ is the neutral gas mass, $v_d$ is the ion drift velocity and $k_B$ is the Boltzmann’s constant. The calculations are performed with the Fortran code gc.f90 [9], which relies on the Gram–Charlier series [4] and uses the matrix elements of the three-temperature theory of gaseous ion transport [31,32]. The details of the numerical computations are very similar to those described in our previous CHe$^+$ paper [5] and in Tuttle et al. [6].

In order to test the reliability and consistency of the present interaction potentials, we have first of all chosen to compute the reduced mobility coefficients of N$^+$ in Ne at room temperature, namely at $T \approx 300$ K. The obtained results of the quantum-mechanical and classical mobilities, as a function of the ratio $E/N$ and as a function of $T_{\text{eff}}$, are shown in Figure 3. They are also compared in the same plot with the experimental measurements of Ellis et al. [33] at 300 K, of Fahey et al. [34] and Viehland et al. [35] at 299 K, of Grice et al. [36] at 298 K, and of McFarland et al. [37] at 297 K. At room temperature, both quantum and classical methods produced the same mobility values that are in a very good agreement with the experimental data of Fahey et al. [34] and Viehland et al. [35]. The concordance is mainly observed for $E/N \geq 10$ Td, where 1 Td = $10^{-21}$ V m$^2$.

Moreover, as Figures 3a and 3b clearly displays, the reduced mobility coefficients based on quantal and classical potential-energy curves, SO effects included, approach at very weak $E/N$ the value $21.04$ cm$^2$ V$^{-1}$ s$^{-1}$, as the electric field increases in intensity, the present N$^+$ ($^3P$) mobility results reach a maximum values that lie between 40 and 60 Td, which are believed typical for mobilities of light ions in helium [34,35]. In addition, as already emphasized by Fahey et al. [34], the zero-field mobilities in He show they are, in general, substantially different from the polarization limit $K_{\text{pol}} = 17.34$ cm$^2$ V$^{-1}$ s$^{-1}$. This fact indicates that, for ions at room temperatures, the Langevin approximation [1] is poor for the weakly-polarisable helium. Theoretically, the polarization limit is attained when the electric field and the gas temperature are low enough, i.e., $(E \rightarrow 0)$ and $(T \rightarrow 0)$ [1].

Being satisfied with the generated results at room temperature, all the quantal and classical calculations of the reduced mobilities, with and without SO effects, in connection with the diffusion of the ground N$^+$ ($^3P_J$) ions in helium gas at 4.3 K are displayed in Figures 4a and 4b. They are also contrasted with some experimental and published data. The non-SO values at the same temperature have been computed quantum-mechanically by Lias et al. [38]. They are presented in Figure 4a. At lower $E/N$, the N$^+$ ion mobility values approach the polarization limit.
Quantal and classical non zero-field mobilities of N$^+$ ($^3P$) ions in He as a function of $E/N$ (left side) and as a function of $T_{\text{dr}}$ (right side) at $T = 4.3\,\text{K}$. They are compared with the experimental values from Sanderson et al. [8] and Tanuma et al. [39]. The horizontal dotted lines represent the polarization limit $K_{\text{pol}} = 17.34\,\text{cm}^2\,\text{V}^{-1}\,\text{s}^{-1}$.

The present results are compared with the available published data. They show, in particular, a decrease in the numerical results mainly at the higher temperature when the spin–orbit effects are included.

As with the CHe$^+$ system [5], the present quantal calculations have also been unable to reproduce the shallow minimum found experimentally by Tanuma et al. [39] around $(E/N) \approx 5\,\text{Td}$. As explained by Mason and McDaniel [1] and Matoba et al. [7], this shallow minimum should come from the attractive long-range potential, and the quantum-mechanical orbiting resonances which occur at weak collisional energy. We display in Figures 5a and 5b a comparison of N$^+$ ion mobilities derived from the use of the average diffusion cross sections with those obtained from the diffusion cross sections of $^3P_0$, $^3P_1$, and $^3P_2$ states. For $^3P_0$, both quantal and classical mobility results display a minimum around 50 Td that appears unrelated to the shallow minimum of experimental data around 5 Td; the $^3P_1$ and $^3P_2$ cross sections show quite different behaviour. It has been argued by Matoba et al. [7] that calculations of the mobility of the C$^+$ ($^2P$) ion in He gas at 4.3 K might show a mobility minimum if the cross sections were computed quantum-mechanically (occurring of the orbiting resonances at low energy), rather than by using the classical-mechanical. Nevertheless, the quantal study of CHe$^+$ system [5] did not find this minimum; consequently, it seems unlikely that it could be present here.

This discrepancy between theory and experiment remains at present unresolved. One could speculate that the experimental measurements of Sanderson et al. [8], and Tanuma et al. [39], realized with the same drift-tube, are unreliable. Tuttle et al. [6] suggest that for the mobility of C$^+$ ($^2P$) in helium gas at 4.3 K i.e., the complexation of the light ion with He during the drift region followed by rapid collisional break-up could lead to a slight slowing of the passage of ion down the drift tube, and hence to lower mobilities.
Table 4. Zero-field reduced mobility $K_0$ and diffusion coefficients $D$ at $T = 4.3$ K and room temperature $T = 300$ K. The diffusion coefficients are given as $D$ times the pressure $p = 0.250$ torr and the gas density $N$.

| Coefficients | $T = 4.3$ K | $T = 300$ K | Refs.     |
|--------------|--------------|--------------|-----------|
| $pD$ (cm$^2$ Torr$^{-1}$) | Without SO | 0.082 | 462.6 | This work |
|               | With SO     | 0.082 | 457.2 |          |
|               |             |       | 432.0 | Fahey et al. [34] |
| $ND$ (10$^{19}$ cm$^{-1}$ s$^{-1}$) | Without SO | 0.018 | 1.489 | This work |
|               | With SO     | 0.018 | 1.495 |          |
|               |             |       | 1.462 | Fahey et al. [34] |
| $K_0$ (cm$^2$ V$^{-1}$ s$^{-1}$) | Without SO | 18.16 | 21.05 | This work |
|               | With SO     | 18.14 | 21.04 |          |
|               |             |       | 20.50 ± 1.00 | Fahey et al. [34] |
|               |             |       | 20.00 ± 1.20 | McFurland et al. [37] |

Fig. 5. State contributions to quantal and classical non zero-field mobilities of N$^+$ ($^3P$) ions in He as a function of $E/N$ at $T = 4.3$ K. They are compared with the experimental values from Sanderson et al. [8] and Tanuma et al. [39]. The horizontal dotted lines represent the polarization limit $K_{pol} = 17.34$ cm$^2$ V$^{-1}$ s$^{-1}$.

5 Conclusion

In this work, the mobility coefficients of N$^+$ ions moving in a ground buffer gas made of helium have been computed using high-level ab initio methods, both with and without the inclusion of spin–orbit coupling, together with both quantum-mechanical and semiclassical computations of momentum-transfer cross sections and their behaviour with energy. Furthermore, within the Gram–Charlier approach, the coefficients of mobility at 4.3 K and their variation with the ratio $E/N$ of the electric field strength to the gas number density of helium have been analyzed. The calculations show that there is only a very small sensitivity to the spin–orbit interaction, and that its introduction does not reproduce the experimentally observed low mobility at low field strengths.

The authors are very grateful to Dr. K. Alioua for his constructive comments. Special thanks are sent, mainly from M.B., to Dr. Larry A. Viehland, from Chatham University, Pittsburgh, PA, USA, for providing his Fortran codes pc.f90 and gc.f90. The latter program has been used in the main parts of the present calculations.

Author contribution statement

Lamia Aïssaoui and Moncef Bouledroua computed the quantum and classical transport cross sections and transport coefficients. Lamia Aïssaoui and Peter Knowles designed and carried out the electronic structure computations, and wrote the first draft of the manuscript. All authors contributed to the final version of the manuscript.

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