SN 2009ip and SN 2010mc as dual-shock Quark-Novae

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Abstract In recent years a number of double-humped supernovae (SNe) have been discovered. This is a feature predicted by the dual-shock Quark-Nova (QN) model where an SN explosion is followed (a few days to a few weeks later) by a QN explosion. SN 2009ip and SN 2010mc are the best observed examples of double-humped SNe. Here, we show that the dual-shock QN model naturally explains their light curves including the late time emission, which we attribute to the interaction between the mixed SN and QN ejecta and the surrounding circumstellar matter. Our model applies to any star (O-stars, luminous blue variables, Wolf-Rayet stars, etc.) provided that the mass involved in the SN explosion is $\sim 20 M_\odot$ which provides good conditions for forming a QN.

Key words: circumstellar matter — stars: evolution — stars: winds, outflows — supernovae: general — supernovae: individual (SN 2009ip, SN 2010mc)

1 INTRODUCTION

SN 2009ip was first discovered as a candidate supernova (SN) by Maza et al. (2009). It was later shown to be consistent with luminous blue variable (LBV) type behavior (Miller et al. 2009; Li et al. 2009; Berger et al. 2009) and dubbed an “SN imposter” as SN 2009ip went through a series of explosions over the next three years resulting in a re-brightening by as much as three magnitudes in the $R$-band (Smith et al. 2011; Pastorello et al. 2013). In early August 2012, the light curve (LC) of SN 2009ip increased to $M_R \sim -15$, brighter than any other outburst, and subsequently decayed over the next 40 days. On 2012 September 23, SN 2009ip re-brightened a final time, peaking at $M_R \sim -18$ and followed an LC similar to type IIn SNe (Smith et al. 2013a). For SN 2009ip, the August event (2012a), followed by the September event (2012b), was the clearest evidence of a double-hump in the LC of an SN so far reported.

SN 2010mc was discovered by Ofek et al. (2013) and also exhibited a precursor outburst (2010a) $\sim 40$ d before the main type IIn event (2010b). Smith et al. (2013b) was the first to comment on the remarkable similarity between the SN 2009ip and SN 2010mc events, both in terms of LC and spectral evolution. However, as far as we know, no pre-SN outbursts were observed in the years prior to the SN 2010mc event as was the case in SN 2009ip. Owing to their uncanny similarity it is natural to conclude that SN 2009ip and SN 2010mc underwent similar processes at the end of their lives.

A debate on what to make of the SN 2009ip events in 2012 (and by association SN 2010mc) is currently underway in the literature. Several theories on the nature of the double-hump in the LC have emerged over the past year either claiming that the 2012 event was a true core-collapse SN, or
simply more intense outbursts like those seen in the three years prior. Several groups (e.g. Mauerhan et al. 2013; Smith et al. 2013a; Prieto et al. 2013) advocate that the first event (2012a) was a core-collapse SN while the second (2012b) was the interaction of the SN ejecta with the circumstellar matter (CSM). Fraser et al. (2013) and Pastorello et al. (2013) argue in favor of the pulsational pair instability (PPI) mechanism in which the double-hump is explained through colliding shells of ejecta caused by two separate PPI explosions. Margutti et al. (2013) also support a two explosion scenario, concluding that the 2012b event was caused by the shock of the second explosion interacting with the material ejected from the first. However, they do not come to a consensus on the nature of the two explosions. Finally, the binary merger hypothesis was put forth by Soker & Kashi (2013) and Kashi et al. (2013) in which the multiple outbursts of SN 2009ip were caused by an interaction of the binary system at periastron. The final 2012b event in their model was the merger of the two stars in what they dub a “mergerburst.”

In this paper we present an alternative explanation for the double-hump in the LC of SN 2009ip and SN 2010mc: the dual-shock Quark Nova (dsQN). This two-explosion scenario was first put forth to explain the LC of SN 2006gy (Leahy & Ouyed 2008; Ouyed et al. 2012) and later successfully applied to other super-luminous SNe (SLSNs) such as SN 2005ap, SN 2006tf, SN 2007bi, SN 2008es, SN 2008fx, PTF09end, PTF10cwr, SN 2010gx (Kostka et al. 2012; Ouyed & Leahy 2009) and SN 2006oz (Ouyed & Leahy 2013); the latter showed evidence of a double-hump. The double-hump is a key feature of the dsQN model and it was predicted in 2009 that future observations of SNe would show this in their LC (Ouyed et al. 2009). The paper is organized as follows: in Section 2 we give an overview of the dsQN model, in Section 3 we show the results of applying the dsQN model to SN 2009ip and SN 2010mc. We end with a discussion and conclusion in Section 4.

2 QUARK NOVA MODEL

A Quark Nova (QN) is an explosive event resulting from the transition of a neutron star (NS) to a quark star1 (Ouyed et al. 2002); see Ouyed et al. (2013) for a recent review. It was suggested that this conversion, combined with the ensuing core collapse of the NS, would result in an explosion causing on average $M_{\text{QN}} \sim 10^{-3} M_\odot$ of neutron-rich material to be ejected with $> 10^{52}$ erg of kinetic energy (Keränen et al. 2005; Ouyed & Leahy 2009; Niebergal et al. 2010).

In core-collapse SNe, neutrinos carry away 99% of the star’s binding energy and drive the explosion. In QNe, neutrinos emitted from the quark core have diffusion timescales exceeding $\sim 10$ ms (e.g. Keränen et al. 2005) and cannot escape before the entire star converts to strange quark matter. For a QN, the agent of explosion is therefore photons, since the temperature of the quark core is large enough at the time of formation (much above the quark plasma frequency) to sustain large photon emissivities (Vogt et al. 2004). The mean free path is small enough to thermalize these photons inside the quark core and in the hadronic envelope so that energy deposition by photons is very efficient. For temperatures from $\sim 1$ to $10$ s of MeV, the photon flux is a few orders of magnitude higher than the neutrino flux from hot quark matter. The energy deposition in the outer layers of the NS (including the crust) is therefore much more efficient for photons than neutrinos and allows for ejecta with kinetic energy easily exceeding $10^{52}$ erg.

The fact that a few percent of the gravitational and conversion (from neutrons to quarks) energy is released as photons is unique to the QN (Ouyed et al. 2005). Even a few percent of the photon energy, when deposited in the thin crust of the NS, will impart a large momentum to it, leading to strong, ultra-relativistic mass ejection (Ouyed & Leahy 2009). The fate of this relativistic ejecta

1 The recent observations of a $\sim 2 M_\odot$ NS (Demorest et al. 2010) do not rule out the existence of quark stars. Heavy quark stars may exist, so long as the strong coupling corrections are taken into account (Alford et al. 2007). Furthermore, NSs and quark stars can co-exist since not all NSs will be converted by the capture of cosmic-ray strangelets (Bauswein et al. 2009). Combining their simulations of strange star binary mergers with recent estimates of stellar binary populations, Bauswein et al. (2009) conclude that an unambiguous detection of an ordinary NS would not rule out the strange matter hypothesis.
DSQN model include the time delay between SN and QN (\(t_{SNQ}\)). We call this time delay an inner radius for the CSM which is equivalent to a time delay for the CSM interaction after the energy of the SN (\(E_{SN}\)) and the velocity of the SN ejecta at \(t = t_{SN}\) is the time for the QN ejecta to catch up to and for the resulting QN shock to propagate through the SN ejecta; the relativistic QN ejecta catches up to the SN ejecta on a very short time scale, \(\sim (v_{SN}/c)t_{delay}\) where \(c\) is the speed of light.

### 3 RESULTS

We fit the LCs of SN 2009ip and SN 2010mc using a three component model: the SN, dsQN and wind. The SN and QN models are those used in Leahy & Ouyed (2008). The key parameters in the SN model are the radius of the progenitor star (\(R_\star = 30M_\odot\)), the mass of the SN ejecta (\(M_{SN}\)), the energy of the SN (\(E_{SN}\)) and the velocity of the SN ejecta (\(v_{SN}\)). The additional parameters of the dsQN model include the time delay between SN and QN (\(t_{delay}\)), the velocity of the QN shock (\(v_{QN, shock}\)) and the energy of the QN explosion (\(E_{QN} = 10^{52}\) erg). The LCs show clear evidence of emission beyond the two humps which is explained in our model as the collision of the combined SN/QN ejecta with the surrounding CSM. To this effect, we use the analytical bolometric LC model of Moriya et al. (2013) since these models are shown to agree well with numerical LCs. These models assume a constant CSM (i.e. wind) velocity \(v_w\) and a CSM density profile \(\rho_{CSM} = Dr^{-s}\) where \(D\) is a constant. The corresponding mass-loss rate is \(\dot{M}_w = \rho_{CSM}v_w 4\pi r^2 = Dv_w 4\pi r^{2-s}\) with the \(s = 2\) case corresponding to the steady mass-loss scenario where \(D = \dot{M}_w/4\pi v_w\). The combined SN/QN ejecta is defined by its kinetic energy \(E_{SNQ}\) and its mass \(M_{SNQ} = M_{SN}(M_{QN} \ll M_{SN})\). Its has a double power-law profile for the density of homologously expanding ejecta (\(\rho_{eq} \propto r^{-n}\) outside and \(\rho_{eq} \propto r^{-\delta}\) inside). Another parameter in these models is the conversion efficiency from kinetic energy to radiation, \(\epsilon\). We assume an inner radius for the CSM which is equivalent to a time delay for the CSM interaction after the SN. We call this time delay \(t_{CSM}\). For each fit, we use \(n = 7\), \(\delta = 0\) and \(\epsilon = 0.1\). We refer the interested reader to section 2.2 in Moriya et al. (2013) for the equations and parameters we used in our modeling of the CSM interaction.
We fit the three component model (SN, dsQN and wind) to the observations by computing models for a variety of parameters until we find parameters that give a combined LC which agrees well with the observations. The time required to generate a model does not allow for an efficient high precision parameter search, and so the parameters represent a good manually-obtained fit rather than the “best fit” from minimizing $\chi^2$.

### 3.1 SN 2010mc

The LC fit of SN 2010mc using the three component model described above is shown in Figure 1 alongside the observations from Ofek et al. (2013). The SN and dsQN models fit the first two humps well and the CSM model fits the late-time LC from $\sim$ day 130 onwards. To produce the fit, we required $M_{SN} = 20 \, M_\odot$, $v_{SN} = 3000 \, \text{km s}^{-1}$, $t_{\text{delay}} = 33 \, \text{days}$ and $v_{QN,\text{shock}} = 8000 \, \text{km s}^{-1}$. We also required a wind velocity of $v_w = 1000 \, \text{km s}^{-1}$ leading to a modest mass loss rate for the wind of $\dot{M}_w \sim 5 \times 10^{-7} \, M_\odot \, \text{yr}^{-1}$.

### 3.2 SN 2009ip

We fit the LC of SN 2009ip using the three-component model in the left panel of Figure 2. The observations plotted alongside our fit are from Smith et al. (2013a). The parameters used in this fit are $M_{SN} = 25 \, M_\odot$, $v_{SN} = 3600 \, \text{km s}^{-1}$, $t_{\text{delay}} = 40 \, \text{days}$, $v_{QN,\text{shock}} = 11000 \, \text{km s}^{-1}$ and $v_w = 2000 \, \text{km s}^{-1}$ leading to $\dot{M}_w \sim 2 \times 10^{-7} \, M_\odot \, \text{yr}^{-1}$. The first and second hump are fitted well by the SN and dsQN model, as in the case of SN 2010mc, but the CSM wind model fails to account for the late-time LC until $\sim$ day 300. This implies the presence of a fourth component, active between $\sim$day 80–300. SN 2009ip went through several violent explosions in the three years prior to the 2012a event resulting in (presumably) dense shells of CSM. Our fourth component is therefore the interaction of the SN/QN ejecta with one of these dense shells. We model the shell using the same prescription above, only with $s = 0$ instead of $s = 2$. The right panel of Figure 2 shows the result of adding this fourth component to the model which significantly improves the model fit. The parameters for the SN 2009ip and SN 2010mc fits are summarized in Tables 1 and 2.

| Source         | $M_{SN}$ ($M_\odot$) | $E_{SN}$ ($10^{50}$ erg) | $v_{SN}$ (km s$^{-1}$) | $t_{\text{delay}}$ (d) | $v_{QN,\text{shock}}$ (km s$^{-1}$) |
|----------------|----------------------|--------------------------|------------------------|------------------------|----------------------------------|
| SN 2009ip      | 20                   | 2.0                      | 3600                   | 40                     | 11000                            |
| SN 2010mc      | 25                   | 4.5                      | 3000                   | 33                     | 8000                             |

| Source          | $D$                  | $s$          | $t_{\text{CSM}}$ (d) | Possible Progenitor |
|-----------------|----------------------|--------------|----------------------|---------------------|
| SN 2009ip (wind)| $5.0 \times 10^3$ g cm$^{-1}$ | 2           | 120                  | LBV star            |
| SN 2009ip (shell)| $1.0 \times 10^{-5.5}$ g cm$^{-3}$ | 0           | 80                   | O-star              |
| SN 2010mc (wind)| $2.5 \times 10^{10}$ g cm$^{-1}$ | 2           | 90                   | O-star              |
**SN 2009ip and SN 2010mc as Dual-Shock Quark-Novae**

**Fig. 1** dsQN model fit (red solid line) to the light curve of SN 2010mc. The observations (black open circles) are from Ofek et al. (2013). The green dotted line represents the SN light curve, the blue dashed line the interaction between the QN and SN ejecta and the magenta dash-dotted line represents the interaction between SN/QN ejecta and the CSM wind.

**Fig. 2** dsQN model fit (red solid line) to the light curve of SN 2009ip. The observations (black open circles) are from Smith et al. (2013a). The green dotted line represents the SN light curve, the blue dashed line the interaction between the QN and SN ejecta and the magenta dash-dotted line represents the interaction between SN/QN ejecta and the CSM wind. The left panel is a 3-component fit to the data whereas the right panel shows a fit using an additional CSM shell component (black dash-dot-dotted line).

### 4 DISCUSSION AND CONCLUSIONS

In our model, the initial hump observed in the LC of SN 2009ip and SN 2010mc is caused by the SN explosion. The second hump is the re-brightening caused when the QN ejecta catches up to and collides with the SN ejecta and the LC tail is a consequence of the SN/QN material interacting with the CSM wind.
Using the dsQN model, we have been able to account for the double-hump in the LC of both SN 2009ip and SN 2010mc. The two humps are fitted with very similar parameters, owing to their remarkably similar LCs. The late time LC of SN 2009ip does not fit well with a single CSM wind model and requires the interaction with a CSM shell of constant density. SN 2009ip went through several LVB-like outbursts in the years prior to the 2012 event so the existence of these shells is expected. For a shell velocity of $\sim 600$ km s$^{-1}$ (Smith et al. 2013a), $v_{SN} = 3600$ km s$^{-1}$ and a $t_{CSM} = 80$ days (both fit parameters from this work) we can infer that the shell was ejected $\sim 400$ d prior to the SN explosion. This places the mass ejection event $\sim$ July 2011, right in the middle of the 2011 outburst (Pastorello et al. 2013). Given the multiple outbursts prior to 2012, it is likely that many such shells exist (Margutti et al. 2013). We choose to only include one interaction in this work to illustrate the idea, although adding more would certainly improve the fit to the LC (and increase the number of free parameters). We should note that we did not need a shell component in our model of SN 2010mc, suggesting that it did not suffer violent mass ejections prior to the 2010 event on the same level as SN 2009ip. This seems to be supported by the fact that no pre-burst activity was detected for SN 2010mc (although absence of proof is not proof of absence). We therefore suggest that the progenitor of SN 2010mc was not necessarily an LBV star (as is the general consensus for SN 2009ip), but could have been an O-star. This is consistent with the QN scenario, in that the type of progenitor is not a concern, as long as it explodes with a low enough mass to leave behind a massive NS (i.e. a QN progenitor) rather than a black hole.

Margutti et al. (2013) argue that a double explosion is needed to explain the observations of SN 2009ip, while Smith et al. (2013a) provide strong evidence that the 2012a event was an SN. Most authors agree that the tail of the LC is supported by interaction between ejecta. Martin et al. (2013) find significant fluctuations during the decline of the SN 2009ip LC past the main peak. They argue against the CSM interaction hypothesis and suggest that these fluctuations may be caused by the progenitor of SN 2009ip which survived its last outburst. In our model, where the CSM interaction comes after the double-hump, these bumps are indicative of the SN/QN material interacting with the different shells ejected during the pre-2012 eruptions. It is natural, in this context, that the fluctuations are consistent with those detected before 2012a since they are essentially an “explosion” echo of the previous bursts. These bumps should be observed in the LC of all dsQNe where the progenitor was an LBV star with relatively recent eruptions.

Our dsQN model provides a natural unifying framework which compliments each of these points. Further, the similarity between the LCs of SN 2009ip and SN 2010mc is simply a consequence of their similar time-delays. No fine tuning of parameters is needed to explain their coincidence. The key ingredient is a progenitor in the right mass range to produce a massive enough NS but not a black hole (i.e. a progenitor leading to an SN ejecta with $M_{SN} \sim 20 M_\odot$ according to our findings).

In summary, we have learned that regardless of the nature of the star (O-star, LBV-star, etc.), if the mass of the ejected envelope in the SN is $\sim 20 M_\odot$, the core seems to meet the conditions to produce an NS massive enough to experience a QN explosion within weeks. These different stars would lead to a variety of SNe (the first hump) and late time emission. The brightness and shape of the second (i.e. QN) hump mainly depends on the time delay between the SN and QN (Leahy & Ouyed 2008; Ouyed et al. 2009).

With so many possible theories being presented in the literature, how can we prove/disprove the dsQN hypothesis? The QN has several unique signatures that are not expected in other models:

1. **Aligned rotator:** The conversion of an NS to a quark star aligns the magnetic field with the axis of rotation (Ouyed et al. 2004, 2006). A radio pulsar is therefore not expected at the location of SN 2009ip and SN 2010mc. However, if beaming is favorable, a parent radio pulsar should be detectable in the period between the SN event and the QN event, particularly once the SN hump is on the decline.
SN 2009ip and SN 2010mc as Dual-Shock Quark-Novae

(2) AXPs/SGRs: If some of the QN ejecta fell back and remained in orbit around the quark star, we would expect to see AXP/SGR behavior around SN 2009ip and SN 2010mc (Ouyed et al. 2007a,b).

(3) R-process elements: The QN provides the ideal site for the creation of r-process elements with atomic weight $A > 130$ (Jaikumar et al. 2007). We should therefore expect to see evidence of these heavy elements in the late-time spectra of SN 2009ip and SN 2010mc.

(4) Neutron decay: Since the QN is an explosion of an NS, a large fraction of the ejecta is composed of free neutrons. Free neutrons decay in $\sim 900$ s (longer if they are relativistic) with unique electromagnetic signatures (see e.g. Severijns 2006; Nico et al. 2006). We therefore expect to see a release of energy soon ($\sim$ hours) after the QN explosion. The exact nature of this signature is still unknown, but may occur at energies $> 15$ keV (assuming it is not absorbed by overlying SN material).

(5) Gravitational waves: In the QN scenario, there are two violent explosions (the SN and QN) that will give distinct gravitational wave signatures (Staff et al. 2012). Future gravitational wave observations of an SN exhibiting a double-hump LC could shed light on the explosion mechanism.

(6) The first hump (the SN) should show signatures of typical SN r-process elements (e.g. Takahashi et al. 1994) while the second hump should include much heavier r-process elements (with $A > 130$) deposited by the QN ejecta (Jaikumar et al. 2007). The QN ejecta is of the order of $10^{-3} M_\odot$ which should yield heavy elements in amounts exceeding the $10^{-6} M_\odot$ values processed in a typical SN.

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