Performance of the Load-in-the-Loop Single Op-Amp Voltage Controlled Current Source from the Op-Amp Parameters

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Abstract. In recent years, Electrical Bioimpedance (EBI) methods have gained importance. These methods are often based on obtaining impedance spectrum in the range of $\beta$-dispersion, i.e. from a few kHz up to some MHz. To measure EBI a constant current is often injected and the voltage across the tissue under study is recorded. Due to the performance of the current source influences the performance of the entire system, in terms of frequency range, several designs have been implemented and studied. In this paper the basic structure of a Voltage-Controlled Current Source based on a single Op-Amp in inverter configuration with a floating load, known as load-in-the-loop current source, is revisited and studied deeply. We focus on the dependence of the output impedance with the circuit parameters, i.e. the feedback resistor and the inverter-input resistor, and the Op-Amp main parameters, i.e. open loop gain, CMRR and input impedance. After obtaining the experimental results, using modern Op-Amps, and comparing to the theoretical and simulated ones, they confirm the design under study can be a good solution for multi-frequency wideband EBI applications because of higher values of the output impedance than 100k\ohm at 1MHz are obtained. Furthermore, an enhancement of the basic design, using a current conveyor as a first stage, is proposed, studied and implemented.

1. Introduction
Given the number of applications of wideband EBI spectroscopy arisen recently in several medical fields such as skin cancer detection [1] or organ transplantation [2], researching and developing new EBI measurement systems with the upper limit frequency as high as possible is required. Hence and due to the current source is an essential block of these systems, several more complex approaches have been proposed aiming to improve their performances in terms of frequency range. Unfortunately, the performance of all these complex approaches degrades markedly near or below 1MHz.

On the other hand, advances in the development of integrated circuits have provided new wide-bandwidth Op-Amps. Therefore, in this paper a simple structure based on a simple, single Op-Amp based circuit topology to operate as a Voltage-Controlled Current Source (VCCS) in wide-bandwidth EBI applications is revisited. Furthermore, an enhancement of this structure is also proposed, studied and tested.
2. Theoretical Analysis
As previously mentioned, current sources are an essential block of EBI systems. Ideally, a current source generates an electrical signal with constant current amplitude independently of the load at any frequency. That means the value of the output impedance, $Z_{out}$, must be infinite at all frequencies [3]. In practice, the value of the $Z_{out}$ is not infinite and it is frequency-dependent. Therefore, the main aim is to achieve current sources with a large output impedance value for a frequency range as wide as possible.

Thus, in this section the output current, $I_{out}$, and the output impedance of both structures are obtained mathematically and their dependences in terms of several parameters are studied. The first structure is a basic structure based on a single Op-Amp in inverting configuration with floating load, also known as load-in-the-loop current source [4]; see figure 1. The other is based on an enhancement of the first one. It consists of adding a first stage based on a VCCS implemented by a current conveyor (CCII) [4]; see figure 2.

2.1. A Single Op-Amp VCCS: Load-in-the-Loop Current Source
To carry out a detailed and realistic analysis of the circuit, a non-ideal operational model of Op-Amp has been selected. It takes into account a finite value of the differential and common-mode input impedance, $Z_d$ and $Z_c$, respectively, a non-zero output impedance, $Z_o$, and a non-zero common-mode gain, $A_{cm}$. Furthermore, it also considers the differential-mode gain and the common-mode rejection ratio are frequency-dependent, $A_d(s)$ and $CMRR(s)$ respectively.

Therefore, given the aforementioned considerations, the circuit under study can be analyzed.

2.1.1. The output current, $I_{out}$
It is given by the ratio between $V_s$ and $R_{in}$, see (1). $R_{in}$ is then the transconductance of the Load-in-the-loop current source.

$$I_{out} \approx I_{in} = \frac{V_s}{R_{in}}$$  

2.1.2. The output impedance, $Z_{out}(s)$
To find the output impedance of the circuit, the voltage source, $V_s$, and the load, $Z_{load}$, are replaced for a short circuit and an auxiliary voltage source, $V_s$, respectively. Furthermore, the overall input impedance of the Op-Amp, $Z_{in}$, can be written as (2). Therefore, given the simplified circuit shown in figure 3, the expression for the output impedance can be written as (3),

$$Z_{in} = \left( Z_d + 2Z_c \right)$$  

$$Z_{out}(s) = \left( \frac{A_d(s)}{s} \right)Z_{in}$$
\[ Z_{\text{out}}(s) = R_{\text{safe}} + R_f \left( Z_o + \left( R_{\text{in}} \right) \cdot \text{opz}(s) \right) \]  

where \( \text{opz}(s) \) is the Op-Amp Impedance factor and is defined as (4).

\[ \text{opz}(s) = 1 + A_d(s) \cdot \left( 1 - \frac{1}{2 \cdot \text{CMRR}(s)} \right) \]  

Figure 3. Equivalent circuit used to calculate the output impedance of the Load-in-the-Loop Current Source.

Figure 4. Equivalent circuit used to calculate the output impedance of the Current-Driven VCCS.

2.2. Current-Driven VCCS

The second proposed circuit consists basically on replacing the Thevenin source, \( V_s \), by a Norton source, i.e., the CCII shown in figure 2. Thus, the output current, \( I_{\text{out}} \), is generated independently of any element related to \( Z_{\text{out}}(s) \). Furthermore, the output impedance of this circuit is essentially proportional to the features of the active devices instead of the input resistor, \( R_{\text{in}} \). This allows to overcome the intrinsic limitation posed by the fact that \( R_{\text{in}} \) cannot be arbitrarily high given that it defines the transconductance of the VCCS.

2.2.1. The output current, \( I_{\text{out}} \). It is approximately equal to the output current in node Z of the CCII; see figure 2. Therefore, it is the same current flowing through node X [5] and it is independent of the input resistor, \( R_{\text{in}} \); see (5).

\[ I_{\text{out}} \approx I_Z = I_{\text{in}} = \frac{V_s}{R_X + R_{\text{in}} \cdot AD844} \]  

2.2.2. The output impedance, \( Z_{\text{out}}(s) \). After simplifying the proposed circuit into the circuit shown in figure 4, the expression for the output impedance, \( Z_{\text{out}}(s) \), can be written as (6)

\[ Z_{\text{out}}(s) = R_{\text{safe}} + R_f \left( Z_o + \left( \left( R_{\text{in}} + Z_{TZ} \right) \right) \cdot \text{opz}(s) \right) \]  

where \( Z_{TZ} \) is the output impedance of the CCII and its value is much higher than the input resistor, \( R_{\text{in}} \).

3. Measurements and Results

To measure the output impedance of both configurations the Impedance Analyzer LCR HP4192A is used in Gain/Phase measurement mode and the technique used by Bertemes-Filho [6] is applied.

On the other hand, the integrated circuits used as the Op-Amp and the CCII are, respectively, LMH6654 by National Semiconductor and AD844 by Analog Devices. Furthermore, the values used for calculating the output impedance magnitude are shown in Table 1.
Table 1: Values & Expressions used for calculating the $Z_{out}$ magnitude.

| Symbol | Expression | Values | Symbol | Values |
|--------|------------|--------|--------|--------|
| $Z_d$  | $R_{id} // C_{id}$ | $R_{id} = 20k\Omega, \quad C_{id} = 0.55pF$ | $Z_o$  | $80\Omega$ |
| $Z_c$  | $R_{cm} // C_{cm}$ | $R_{cm} = 4M\Omega, \quad C_{cm} = 0.9pF$ | $R_{in}$ | $6.2k\Omega$ |
| $A_d(s)$ | $A_d(s)/(1+(s/\omega_d))$ | $A_d = 67dB, \quad \omega_d = 2\pi \cdot 125kHz$ | $R_{safe}$ | $390\Omega$ |
| $CMRR(s)$ | $CMRR(s)/(1+(s/\omega_{cm}))$ | $CMRR = 90dB, \quad \omega_{cm} = 2\pi \cdot 9kHz$ | $R_f$  | $390k\Omega$ |
| $Z_{TZ}$ | $R_{TZ} // C_{TZ}$ | $R_{TZ} = 3M\Omega, \quad C_{TZ} = 4.5pF$ |   |   |

Therefore, the measured output impedance values from the experimental tests are shown in figure 5 and figure 6.

Figure 5. Plotted output impedance for different values of $R_f$. $R_f = 390k\Omega$ and 1.5M$\Omega$. N.B. $R_{in} = 6.2k\Omega$.

Figure 6. Adding a 2.5pF parasitic capacitance in the calculated $Z_{out}$, the measured and the simulated $Z_{out}$ match up. Furthermore, if a 2.5pF capacitor is added to the implemented board, the cut-off frequency becomes smaller.

4. Discussion

4.1. Regarding the feedback resistor, $R_f$
Due to $R_f$ is in parallel with the output of the current source, it acts as current divider of the output current. Furthermore, it limits the maximum value of the output impedance; see figure 5.

Thus, the higher $R_f$ is, the higher the output impedance becomes. But, because of providing a path for the bias current of the Op-Amp is usually required in EBI systems, $R_f$ cannot be removed.

4.2. Regarding the parasitic capacitance, $C_p$
As figure 5 shows, there is a good agreement between the measured and the calculated output impedance in the frequency range below 100 kHz. Above this range, the value of the cut-off frequency varies depending on the value of $R_f$. The higher $R_f$ is, the smaller the cut-off frequency becomes. The main reason is because of the influence of parasitic capacitances, $C_p$, is not negligible at high frequencies. A 2.5pF value of $C_p$ is found as the best value which fits with the measured output impedance.
Hence, the working frequency range for a VCCS is not given only by the Op-Amp features but also by the parasitic capacitances present at the output of the VCCS.

5. Conclusions
As this results show, implementing wideband current sources using a single Op-Amp circuit for spectroscopy measurements of EBI is a realistic approach. Using the Load-in-the-loop Current Source, wideband multifrequency applications can be implemented properly in terms of large output impedance at a very low cost. Furthermore, to achieve an output current of the VCCS more robust and constant and also independent of any element related to the output impedance, the improved circuit called Current-Driven VCCS is proposed.

Therefore, the overall output impedance for both configurations can be plotted as in figure 7. As observed, the overall output impedance is modeled as three impedances building up a parallel bridge: the $Z_{in}$, $Z_i$ and $R_f$. The parameter $Z_{in}$ was defined in (2) as the Op-Amp input impedance. $Z_i$ is the equivalent input impedance from the inverting input of the Op-Amp to ground, i.e. $R_{in}$ in the Load-in-the-loop Current Source and $R_{in}+Z_{TZ}$ in the Current-Driven VCCS. Furthermore, the $opz(s)$ was also defined in (4) as the Op-Amp Impedance factor. The higher these three impedances and the $opz(s)$ are, the higher the overall output impedance becomes. This can help to choose the right Op-Amp from the system requirements.

On the other hand, as previously mentioned, the effect of the parasitic capacitances is the critical factor limiting the performance of the current source at high frequencies. Hence, to improve the performance of the current source, parasitic capacitances should be avoided or minimized as far as possible from the earliest stage of the circuit design. Furthermore, in a real measurement system, a higher capacitance exists due to the coaxial cables connected between the current source and the load. This problem affects all current source structures and can be only overcome if the VCCS is placed near the electrodes or driven guards are used for the coaxial cables. Also dominant pole strategies can be employed to avoid oscillations in that last case.

![Figure 7. Equivalent circuit for the output impedance of both VCCS circuits. The parasitic capacitances’ effect is added in discontinuous trace. N.B. the values of $R_{safe}$ and $Z_o$ are considered negligible.](image)

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