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MODELLING, SIMULATION AND PARAMETER IDENTIFICATION OF ACTIVE POLLUTION REDUCTION WITH PHOTOCATALYTIC ASPHALT

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Abstract. We develop and implement a numerical model to simulate the effect of photocatalytic asphalt on reducing the concentration of nitrogen monoxide (NO) due to the presence of heavy traffic in an urban environment. The contributions in this paper are threefold: we model and simulate the spread and breakdown of pollution in an urban environment, we provide a parameter estimation process that can be used to find missing parameters, and finally, we train and compare this simulation with different data sets. We analyse the results and provide an outlook on further research.

Keywords: pollution; environmental modelling; parameter identification; finite element simulation.

1. INTRODUCTION

Pollution in urban environments has been a major issue for several decades and efforts of combating it have spanned across many areas of research. Emerging technologies, such as those based on photo-catalysis target the removal of vehicular nitrogen oxides (NO\textsubscript{x}) to mitigate the roadside air pollution problem. These techniques have proven effective and research in this area is still ongoing. Recently, a lot has been done from the experimental perspective as well, see i.e. \cite{1} for experimental studies on visible–light activated photocatalytic asphalt, or \cite{2–5} for photo-catalytic concrete products as well as \cite{6} for actual observational studies. A comprehensive overview of the underlying principles in photo-catalysis processes in connection with removal of air pollutants is presented in \cite{7–9} and the references therein. However, from the mathematical modelling and simulation point of view, this setting is less studied. A remotely related situation is handled via a fluid dynamics-based study on the pollutant propagation in the near ground atmospheric layer as discussed in \cite{10}. We strongly believe that there is a need for a deeper insight via mathematical modelling and simulations in the connections between experiments, theory and practical applications of the methodology. This is the place where we wish to contribute. Similar techniques as the ones we apply are detailed in \cite{11}, to which we refer the interested reader for more details on the modelling structure.

In this paper, we report on the use of numerical simulations to mimic the effect of the presence of a street paved with photocatalytic asphalt has on the NO reduction in the local ambient. Comparisons are based on data collected at a neighbourhood of one of the streets in Kiel, Germany. The findings in this work contribute to enhance the understanding on the interplay between the various factors involved in the air pollution control. The contributions of this paper are threefold:

- We model and simulate the spread and breakdown of pollution in an urban environment.
- We provide a parameter estimation process that can be used to determine relevant missing parameters.
- We train and compare this simulation with different data sets.

The paper is structured as follows: first, we present the model equations in a dimensionless formulation and explain what they are describing. Then, we provide an insight in the reference set of parameters we use. As a next step, we use the designed model to formulate and solve a parameter identification problem required to identify the effect of the local environment on the NO evolution. Finally, we compare our numerical results with the measured data from both before and after the photocatalytic asphalt was placed.

2. NO POLLUTION MODEL

2.1. MODEL DESCRIPTION

The urban environment we model is the cross-section of a road. This is a three-lane highway within city limits. In our two-dimensional model, we represent the introduction of the pollution by the cars, which is diffused through the air. We model sunlight as a reactive factor \cite{7,8}. Finally, we model interaction with the rest of the environment by using Robin boundary conditions. These boundary conditions include environmental effects from neighbouring locations (especially molecular diffusion and dispersion), represented in a single parameter later referred to as \(\sigma\). We do
To keep the presentation concise, we introduce the wind effects in our model would necessarily force us with the current data available. Introducing genuine wind by a simple translation of the fluxes with an estimation; (2) our model can handle a slow-to-moderate variation for this is two-fold: (1) we are not aware of values for this coefficient that are of order $10^2$ higher. This brings the numerical output in the range of emission measurements for large ranges of all the other model parameters. To quantify the evolution of the air pollutant, one has to first get a grip on the typical sizes of $\sigma$, $\kappa$ and $\gamma$. The term $\Lambda_s (t)$ represents the contribution from the reaction where NO is converted to NO$_2$ with a reaction rate $\kappa$. The dependence of $\Lambda_s$ on the other parameters is given by $\Lambda_s = \frac{2\kappa L^2}{D}$. The following initial and boundary conditions are imposed on (1).

$$u(x, 0) = \frac{u_0}{u_r} \quad \text{for} \quad x \in \Omega,$$

$$-\nabla u \cdot n = 0 \quad \text{at} \quad \Gamma_N \times (0, 1),$$

$$\nabla u \cdot n = \frac{\sigma L}{D} \left(u - \frac{u_T}{u_r}\right)^+ \quad \text{at} \quad \Gamma_R \times (0, 1),$$

$$\nabla u \cdot n = \frac{\gamma \kappa L}{D} u \quad \text{at} \quad \Gamma \times (0, 1),$$

where $\gamma^+$ denotes the positive part of $\gamma$, namely $g^+(x) = \max(g(x), 0)$ for $x \in \Gamma_R$.

We refer to $\sigma$ as the environmental parameter, to $\kappa$ as the reaction rate and to $\gamma$ as the asphalt reactivity. All parameters can be seen as mass-transfer coefficients; $\sigma$ represents the exchange of NO with the ambient atmosphere, $\kappa$ expresses the speed of the reaction from NO to NO$_2$ while $\gamma$ expresses the capacity of the photo-voltaic asphalt. In our model, we choose a value of $\sigma = 300 \text{ m}^3/\mu\text{g}$, consistent with the base level of NO concentration in the environment according to the measurements. When simulating the scenario prior to the photo-voltaic asphalt, $\gamma = 0$.

It is worth mentioning that $\kappa$ and $\gamma$ are influenced by a multitude of effects, including but not limited
to the local atmospheric conditions, the effect of UV, temperature and humidity and the porosity and the chemical composition of the asphalt. For this reason, these parameters are situation specific and require tuning for each scenario that one wants to model. We will do so by applying a parameter identification technique, described in Section 4.

2.3. OTHER PARAMETERS

2.3.1. INITIAL AND THRESHOLD CONCENTRATIONS OF NO

$u_0$ represents the initial mass concentration of NO present in the environment. In this simulation, we choose a concentration of $u_0 = 37 \, \mu g/m^3$. This value corresponds to the lowest available NO concentration level from the measurements. $u_T$ represents the threshold concentration level from which NO disperses out of the environment we consider. In this model, we choose $u_T = 0 \, \mu g/m^3$, which means we assume low ambient levels of NO, ensuring natural dispersion even at low concentrations. In the case of high ambient levels of NO due to, e.g., nearby factories or other highways, $u_T$ can be higher.

2.3.2. PATCH-WISE VEHICLE DISTRIBUTION

The emission of NO is proportional to the amount of motor vehicles passing through this cross-section. The distribution of motor vehicles is derived from measurements of [13], a German municipal service that performs automated traffic counts for a large number of cities. The traffic count we collect our data from is located at 3.5 kilometers from the NO measuring point. Because the roads in question are similar in size and geographically close, we expect this data to provide a reliable estimate. Daily, 72278 cars passed are counted in both directions of the road. The traffic count is aggregated on an hourly level, so in order to obtain a vehicle distribution, we interpolate the hourly data with cubic splines and normalize the resulting function. We end up with a nominal density $m(t)$ of cars for each time $t \in [0, 1)$ such that $\int_0^1 m(t) \, dt = 1$. A plot of $m(t)$ is presented in Figure 2.

2.3.3. PATCH-WISE NO EMISSION (PER VEHICLE)

We model the emission of NO by choosing a specific shape for the source term $f(x, t)$ from (1). This source term is defined as follows:

$$f(x, t) = \begin{cases} m(t), & \text{if } x \in A, \\ 0, & \text{if } x \notin A, \end{cases}$$

for all $x \in \Omega$ and $t \in [0, 1)$, where $A$ is a rectangle of $15 \times 0.4$ square meters, located 0.1 meter over the asphalt. This box represents the location of the emission of the vehicles. It is illustrated by the grey box in Figure 1.

2.3.4. CROSS-SECTION GEOMETRY

The dimensions of the simulated cross-section (displayed in Figure 1) are 40 meters by 8 meters. In the simulation, the road has a width of 15 meters ($2 \times 3$ lanes of each 2.5 meters wide) and is located in the middle of the cross section. This is a simplified representation of the road under consideration, but can be generalized to model roads of any dimension. The measuring point we use to evaluate the simulated NO concentration profile is located 1.75 meters above the centre of the road, in accordance to the real measuring point that provided us the NO concentration data.
2.3.5. Solar effects on NO
The natural conversion from NO to NO₂ due to sunlight is represented by term $\kappa A_s s(t)$. In this term, the intensity of the UV radiation is expressed by the dimensionless factor $s(t)$. We compute this factor by interpolating the sunrise, sunset and solar noon data from [14] and normalizing to obtain a function $s(t)$ such that $\int_0^1 s(t) \, dt = 1$. This is done under the assumption that there is no UV radiation between sunset and sunrise and that the maximum of UV radiation takes place at solar noon. For our simulation, we choose a reference value $s_r = 1$ UVI (see Appendix), where by UVI we mean the UV Index of the sunlight, a dimensionless quantity. A plot of the shape of $s(t)$ is presented in Figure 3.

2.3.6. Pollution-reducing effects
As mentioned above, the values of $\kappa$ and $\gamma$ strongly depend on the environment. By using the measurement data detailed in the next section, we have enough information to derive the values of these parameters for our model.

3. Measurements
The NO measurements used in the simulation cover a period from 2012 to 2017, where NO was measured in 30-minute intervals. We clean the data by limiting ourselves to a specific period: from September 1st to December 10th: 101 measurements outside of the holiday period, with an average intensity of the sun (between summer and winter). We interpolate this data to obtain the emission profile of an average day. Data in this period from 2017 corresponds to the newly installed photocatalytic asphalt. To compare this scenario with the initial situation, we use the measured data from 2016.

To assert that the traffic intensity remained relatively constant, we compare the measurements from 2016 to the same period in 2015. Figure 4 shows comparable concentration profiles. This indicates, as a reasonable assumption, that the only major change between 2016 and 2017 was the new asphalt, given the local weather conditions incorporated in the parameter $\kappa$. Figure 4 reveals a large reduction in NO pollution after 2016.

4. Parameter identification
As stated in Section 2, we require situation-specific values for the parameters $\kappa$ and $\gamma$. To obtain these, we propose and solve a parameter identification problem based on the datasets described in Section 3. In a two-step procedure, we first use the measurements prior to the installation to obtain $\kappa$, knowing that in this case $\gamma = 0$, and then use the measurements after the installation to obtain $\gamma$.

Mathematically speaking, we wish to solve the following problem: Let $u(\cdot; \kappa, \gamma)$ be the solution to (1) for given parameters $\kappa$ and $\gamma$ and $u_r$ be the measurement data. Find $\kappa$ and $\gamma$ that solve the following optimization problem:

$$
\min_{\kappa \in P_\kappa} \min_{\gamma \in P_\gamma} \left\| u_r(x, t) - u(x, t; \kappa, \gamma) \right\|_{L^2(\Omega \times (0,1))}.
$$

(4)

Here $P_\kappa$ and $P_\gamma$ are compact sets in $\mathbb{R}$ where parameters are searched.

5. Simulation
This section describes the setup of determining the effectiveness of the photocatalytic asphalt.
5.1. Simulation framework

We numerically compute the solution to (1) with (2) with a finite element simulation using the FEniCS library [15]. We investigate the process within the specified cross-section, leading to a two-dimensional reaction-diffusion process. The finite element mesh has $30 \times 30$ elements on a rectangular grid. The solution to (1) is approximated with quadratic basis functions.

We simulate two scenarios: (A) the NO concentration profile prior to the photocatalytic asphalt (corresponding to measurements from 2015 and 2016); and (B) the NO concentration profile after the installation of the photocatalytic asphalt (corresponding to measurements from 2017). In these simulations, we use the parameters as described in Section 2 and choose a diffusion coefficient of $D = 43.8$, which shows an agreement with the current setting. In case (A) specifically, we fix $\gamma = 0$.

Our goal is to use the data set from (A) to train our simulation on the value of parameter $\kappa$. Then we use the data set from (B) to determine the effect corresponding to measurements from 2015 and 2016).
the photocatalytic asphalt has on the reduction of the local NO concentration, i.e., find $\gamma$.

Figure 5 displays this process, where for a range of $\kappa$, we plotted the relative discrepancy with the measurements. More precisely, let $u_r$ denote the interpolation of the measurements and $u_\kappa$ the result of our simulation for a specific $\kappa$, then the relative discrepancy $e_\kappa(u)$ is defined as

$$e_\kappa(u) = \frac{\|u_r - u_\kappa\|_{L^2(\Omega \times (0,1))}}{\|u_r\|_{L^2(\Omega \times (0,1))}}.$$  \hspace{1cm} (5)

Having captured the nature of the process, we can estimate the effect of the photocatalytic asphalt in terms of $\gamma$ by starting a new parameter identification process using the data set from the second scenario.

Figure 6 shows the relative discrepancy (similarly defined as in (5)) for $u_\gamma$ (with an optimal value of $\kappa$). Figure 5 and Figure 6 suggest that we are dealing with a convex minimization problem.

The simulations with optimally fitted parameters, before and after the construction of the photocatalytic asphalt, are displayed in Figure 7.
We use the measurements of NO to compare the simulation results with. Figure 8 shows the measured and simulated data combined. The simulation agrees qualitatively and quantitatively, with a mass error of 58.64 µg/m³ in the pre-photocatalytic case and 22.68 µg/m³ in the post-photocatalytic one. This mass error is defined as

$$\int_0^T \int_\Omega |u(x, t) - u_r(x, t)| \, dx \, dt,$$

where $u$ represents the simulation solution and $u_r$ the measurements.

6. DISCUSSION AND OUTLOOK

This report shows that it is possible to use a mathematical model like the one presented in Section 2 to describe the evolution of NO concentration as a function of time in an urban environment where both intense motorized vehicle traffic and photocatalytic asphalts are present.

A number of things can be done to continue this investigation and improve the quantitative predictions obtained in this study.

• Perform a 3D simulation along the whole length of the photocatalytic asphalt.

• Account for the presence of uncertainties in the weather condition (especially the variation in the UV radiation and the effect of precipitation).

• Numerically identify scenarios leading to an extreme NO pollution.

• By neglecting wind flux, we emphasize that our interest lies in quantifying the reactive part of this reaction-diffusion process. This approach allows us to identify two extreme scenarios: (1) excellent performance of the asphalt, and (2) low-response on NO pollution induced by the presence of the asphalt. Including more detailed wind effects is certainly of an interest (both from a theoretical and a practical perspective), since it is known that the location under investigation (Kiel, Germany) is prone to varied weather conditions.

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8. APPENDIX

For $x \in \Omega$ and $t \in [0, T)$, we consider the following equation

$$\frac{\partial u}{\partial t} - \nabla \cdot (D \nabla u) = f(x, t) - \kappa s(t) u(x, t).$$

Let us also introduce the following rescalings: $\tilde{x} = \frac{x}{L}$, $\tilde{t} = \frac{t}{\tau}$, $\bar{u} = \frac{u}{u_r}$, $\bar{f} = \frac{f}{f_r}$, and $\bar{s} = \frac{s}{s_r}$, where

$$f_r = \max_{(x, t) \in \Omega \times [0, T]} |f(x, t)|.$$

Rewriting (7) using these new rescaled functions and variables yields

$$\frac{\partial \bar{u}}{\partial \tilde{t}} - \frac{\tau D}{L^2} \nabla \cdot (\nabla \bar{u}) = \frac{\tau f_r}{u_r} \bar{f} - \kappa \tau s_r \bar{s} \bar{u}. $$
This equation is posed in a rescaled space domain \( \overline{\Omega} = \frac{\Omega}{L} \). Choosing \( t_r = \frac{L^2}{D} \) reduces (8) to the form

\[
\frac{\partial \overline{u}}{\partial t} - \nabla \cdot (\nabla \overline{u}) = \frac{L^2}{D} \overline{f} - \kappa \frac{L^2}{D} \overline{s} \overline{u}.
\]

(9)

Setting \( A_f = \frac{L^2}{D} \overline{f}, A_s = \frac{L^2}{D} \overline{s} \) and abusing the notation, namely rewriting \( \Omega \) instead of \( \overline{\Omega} \), \( u \) instead of \( \overline{u} \), \( f \) instead of \( \overline{f} \), and \( s \) for \( \overline{s} \) in (9) posed in \( \overline{\Omega} \) gives (1) posed in \( \Omega \). A similar discussion yields the structure of the initial and boundary conditions in a non-dimensional form.

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