Significantly Improved Colossal Dielectric Properties and Maxwell—Wagner Relaxation of TiO$_2$—Rich Na$_{1/2}$Y$_{1/2}$Cu$_3$Ti$_{4+x}$O$_{12}$ Ceramics

Pariwat Saengvong 1, Narong Chanlek 2, Bundit Putasaeeng 3, Atip Pengpad 1,4, Viyada Harnchana 1,4 *, Srirajak Krongsuk 1,4, Pornjuk Srepusharawoot 1,4, and Prasit Thongbai 1,4, *1*

Abstract: In this work, the colossal dielectric properties and Maxwell—Wagner relaxation of TiO$_2$—rich Na$_{1/2}$Y$_{1/2}$Cu$_3$Ti$_{4+x}$O$_{12}$ (x = 0–0.2) ceramics prepared by a solid-state reaction method are investigated. A single phase of Na$_{1/2}$Y$_{1/2}$Cu$_3$Ti$_{4+x}$O$_{12}$ is achieved without the detection of any impurity phase. The highly dense microstructure is obtained, and the mean grain size is significantly reduced by a factor of 10 by increasing Ti molar ratio, resulting in an increased grain boundary density and hence grain boundary resistance ($R_{gb}$). The colossal permittivities of $\varepsilon'$ ~ 0.7–1.4 × 10$^4$ with slightly dependent on frequency in the frequency range of 10$^3$–10$^6$ Hz are obtained in the TiO$_2$—rich Na$_{1/2}$Y$_{1/2}$Cu$_3$Ti$_{4+x}$O$_{12}$ ceramics, while the dielectric loss tangent is reduced to tan$\delta$ ~ 0.016–0.020 at 1 kHz due to the increased $R_{gb}$. The semiconducting grain resistance ($R_g$) of the Na$_{1/2}$Y$_{1/2}$Cu$_3$Ti$_{4+x}$O$_{12}$ ceramics increases with increasing $x$, corresponding to the decrease in Cu$^{4+}$/Cu$^{2+}$ ratio. The nonlinear electrical properties of the TiO$_2$—rich Na$_{1/2}$Y$_{1/2}$Cu$_3$Ti$_{4+x}$O$_{12}$ ceramics can also be improved. The colossal dielectric and nonlinear electrical properties of the TiO$_2$—rich Na$_{1/2}$Y$_{1/2}$Cu$_3$Ti$_{4+x}$O$_{12}$ ceramics are explained by the Maxwell—Wagner relaxation model based on the formation of the Schottky barrier at the grain boundary.

Keywords: colossal/giant dielectric properties; X-ray photoelectron spectroscopy; Maxwell—Wagner relaxation; impedance spectroscopy; NYCTO

1. Introduction

Improvement of electronic device efficiency through the development of materials with enhanced electrical properties is significant. Colossal dielectric oxides (CDOs) with very high dielectric constant ($\varepsilon'$) are widely used to manufacture critical components in electronic devices, especially for multilayer ceramic capacitors (MLCCs) [1–3]. The $\varepsilon'$ of a CDO influences the geometry and performance of the MLCCs. The size of an MLCC can be miniaturized by using the insulating oxide between the metallic electrodes with a dielectric oxide with a higher $\varepsilon'$ value than the conventional oxide. Many CDOs have intensively been investigated, especially for CaCu$_3$Ti$_4$O$_{12}$ (CCTO) and related compounds, expecting to replace traditional CDOs such as BaTiO$_3$—based ceramics.

The dielectric and electrical properties of the perovskite CCTO ceramics have been extensively studied over the past two decades [4–12]. This is because CCTO ceramics showed high $\varepsilon'$ ~ 10$^3$–10$^5$ over wide ranges of temperature and frequency. Moreover, the $\varepsilon'$
of CCTO ceramics are relatively stable in the temperature range of 100–400 K compared to conventional BaTiO₃-based ceramics used. Unfortunately, CCTO still presents too high dielectric loss (\(\tan \delta >> 0.05\)), which is not required for application in MLCCs [13–15]. Therefore, researchers have studied reducing the \(\tan \delta\) of CCTO ceramics by tuning the ceramic microstructure of CCTO and related ceramics according to their heterogeneous electrical structure. The special microstructure, which consists of semiconducting grains and highly resistive boundaries (GBs), can be produced using one-step processing method [5]. This heterogeneous microstructure is called to be an internal barrier layer capacitor (IBLC) structure. Accordingly, the resistivity and correlated \(\tan \delta\) can be improved by engineering the grains and GBs [16,17]. In addition, the presence of insulating GBs affects a nonlinear relationship between current density \((J)\) and electrical field strength \((E)\), which is a behavior required for developing varistor devices [4,9,18].

To improve the colossal dielectric and nonlinear \(J–E\) properties, many effective methods have been proposed and studied, such as doping with suitable ions [19–22], tuning ceramic microstructure [9] and fabricated CCTO–matrix composites [10,18,23,24]. These methods have the same approach, which is to increase the total resistance of the insulating GBs \((R_{gb})\) for reducing \(\tan \delta\). One of the most effective methods is to fabricate the CCTO–matrix composites using an appropriate ceramic filler such as CaTiO₃ (CTO), Al₂O₃ or TiO₂ [6,7,10,18,25]. For the CTO/CCTO and TiO₂/CCTO composites, although the \(\tan \delta\) can be significantly reduced to <0.05, their \(\varepsilon′\) values are usually significantly decreased in the order of 10³. For these two composite systems, the nonlinear electrical properties can also be significantly improved. The TiO₂/CCTO composites can be easily prepared by designing TiO₂–rich phase in the CCTO ceramics using the formula CaCu₃Ti₄⁺ₓO₁₂₊₂x. Notably, the mean grain size was reduced, resulting in a significant increase in \(R_{gb}\). This is the primary cause of the observed improvement of the colossal dielectric and nonlinear electrical properties of CCTO ceramics.

In addition to CCTO ceramics, the colossal dielectric properties of ACu₃Ti₄O₁₂ oxides (\(A = \text{Na}_{1/2}\text{Bi}_{1/2} [26], \text{Na}_{1/2}\text{Y}_{1/2} [27–30], \text{Na}_{1/2}\text{La}_{1/2} [31], \text{Bi}_{2/3} [32,33], \text{Y}_{2/3} [32,34], \text{Cd} [16,17,35], \text{La}_{2/3} [32], \text{Sm}_{2/3} [36], \text{Na}_{1/3}\text{Ca}_{1/3}\text{Bi}_{1/3} [37], \text{Na}_{1/3}\text{Cd}_{1/3}\text{Y}_{1/3} [38], \text{Na}_{1/3}\text{Sr}_{1/3}\text{Y}_{1/3} [39] \) and \(\text{Na}_{1/2}\text{Sm}_{1/2} [40]\) are very attractive, especially for the \(\text{Na}_{1/2}\text{Y}_{1/2}\text{Cu}_{1/2}\text{Ti}_{4}\) (NYCTO) ceramics [27–30]. The NYCTO ceramics exhibited a high \(\varepsilon′ \sim 10^8\) with low \(\tan \delta < 0.05\) at 1 kHz compared to that of the CCTO ceramics [28–30]. Recently, the preparation, colossal dielectric permittivity and nonlinear electrical properties of NYCTO ceramics has been widely reported [27–30,39,41–43].

In this work, the TiO₂–rich NYCTO ceramics were prepared by a conventional mixed–oxide method and investigated the dielectric properties. The crystal structure, phase composition and microstructural evolution of the sintered ceramics, as well as their oxidation states, were characterized. The primary cause of the enhanced colossal dielectric response was systematically elucidated. This study contributes an exciting concept for improving the colossal dielectric properties of the NYCTO ceramics by reducing their \(\tan \delta\). We believe that this research work provides an effective route to improve the CDOs for future applications in MLCCs.

2. Experimental Details

\(\text{TiO}_₂–\text{rich Na}_{1/2}\text{Y}_{1/2}\text{Cu}_{1/2}\text{Ti}_{4+x}\text{O}_{12} (\text{NYCTO}+\text{xTiO}_₂)\) ceramics (where \(x = 0.0, 0.1\) and 0.2) were prepared using solid-state reaction method (SSR). The starting materials were \(\text{Na}_2\text{CO}_3 (99.9\%), \text{Y}_2\text{O}_3 (99.99\%), \text{CuO} (99.9\%)\) and \(\text{TiO}_2 (99.9%)\), which were purchased from Sigma–Aldrich (St. Louis, MO, USA). Details for the preparation of NYCTO–based oxides were provided elsewhere [28,30,39]. The mixed powders for all compositions were calcined at 1000 °C for 10 h. Mixed powders (without calcination) were pressed into 9.5-mm-diameter pellets by uniaxial compression at ~100 MPa. Finally, the pellets were sintered at 1070 °C for 10 h in air. The sintered NYCTO + \(x\text{TiO}_₂\) ceramics with \(x = 0.0\), 0.1 and 0.2 were referred to as the NYCTO, NYCTO + 0.1TiO₂ and NYCTO + 0.2TiO₂, respectively.
The crystal structures of the sintered sample were characterized using X-ray diffraction (XRD, PANalytical, EMPYREAN, Shanghai, China), scanning electron microscopy (MiniSEM, SEC, SNE–4500 M), field emission scanning electron microscopy (FIB–FESEM,) with energy dispersive X-ray (EDX) spectroscopy and X-ray photoemission spectroscopy (XPS, PHI5000 Versarobe II, ULVAC–PHI, Chigasaki, Japan). Comprehensive details were provided in our previous works [12,21,44–46].

For the nonlinear electrical and dielectric measurements, the surfaces of samples were polished. Next, the parallel and smooth surfaces were coated with silver paints and fired in the air at 600 °C for 30 min. The impedance and dielectric parameters of all sintered ceramics were measured with an impedance analyzer (KEYSIGHT E4990A, Santa Rosa, CA, USA). The dielectric properties were measured in the temperature range of −160 to 210 °C and the frequency range from $10^2$–$10^7$ Hz. The nonlinear relationship between current density ($J$) and electrical field strength ($E$) was analyzed by using a high–voltage measurement unit (Keithley 247 model, Cleveland, OH, USA).

3. Results and Discussion

The XRD patterns of the sintered NYCTO + xTiO$_2$ ($x = 0, 0.1$ and $0.2$) ceramics are illustrated in Figure 1a, showing the single phase of NYCTO in all ceramics with a perovskite-structure (JCPDS 75–2188). The crystal structure of NYCTO is demonstrated in Figure 1b. The XRD peak corresponding to TiO$_2$ phase cannot be detected in the NYCTO + 0.1TiO$_2$ and NYCTO + 0.2TiO$_2$ ceramics, which may be due to a small amount of an excess TiO$_2$ molar ratio that was lower than the resolution limit of the XRD technique. Accordingly, the lattice parameters ($a$) can be calculated and found to be 7.383, 7.383 and 7.384 Å for the NYCTO, NYCTO + 0.1TiO$_2$ and NYCTO + 0.2TiO$_2$ ceramics, respectively. The $a$ values are comparable to those reported in the literature [27–30]. The excess TiO$_2$ composition in NYCTO ceramics does not affect the lattice parameter. This result indicates that the TiO$_2$—rich phase is segregated from the primary phase of NYCTO, which may exist as the TiO$_2$—rich boundary. The XRD result shows that the NYCTO + xTiO$_2$ has successfully been fabricated using the SSR method.

Even though the excessive TiO$_2$ phase was not detected in the XRD patterns for all ceramics, the variation in compositions of the CuO and/or TiO$_2$ ratios in an ACu$_3$Ti$_4$O$_{12}$ compound usually affects the dielectric and electrical properties [6,10,24,45,47–49]. Thus, we first investigated the dielectric properties of the NYCTO + xTiO$_2$ ceramics at around room temperature (30 °C). The relationship between the $\varepsilon'$ and frequency of the NYCTO + xTiO$_2$ ceramics is shown in Figure 2a. The $\varepsilon'$ value of the NYCTO ceramic is huge ($2.07 \times 10^4$ at $10^3$ Hz) with a quite low $\tan \delta \approx 0.115$, which is similar to that reported in the previous works [27,28,30]. The excess TiO$_2$ composition in NYCTO ceramics does not affect the lattice parameter. This result indicates that the TiO$_2$—rich phase is segregated from the primary phase of NYCTO, which may exist as the TiO$_2$—rich boundary. The XRD result shows that the NYCTO + xTiO$_2$ has successfully been fabricated using the SSR method.

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Figure 1. (a) XRD patterns of NYCTO + xTiO2 ceramics with x = 0.0, 0.1 and 0.2. (b) NYCTO structure.

Figure 2b illustrates the tanδ at 30 °C for the NYCTO + xTiO2 ceramics over the frequency range of 10²–10⁶ Hz. In the frequency range of 10²–10⁵ Hz, the tanδ values of the NYCTO + 0.1TiO₂ and NYCTO + 0.2TiO₂ ceramics are much lower than the NYCTO ceramic. Furthermore, in this frequency range, the tanδ values of the NYCTO + 0.1TiO₂ and NYCTO + 0.2TiO₂ ceramics are lower than 0.1. The rapid increase in tanδ of all the ceramics is attributed to the primary dielectric relaxation, i.e., Maxwell—Wagner polarization relaxation [12,19]. The tanδ values of the NYCTO, NYCTO + 0.1TiO₂ and NYCTO + 0.2TiO₂ ceramics 10³ Hz are 0.115, 0.020 and 0.016, respectively. Notably, the tanδ value of the NYCTO ceramics can be significantly reduced by increasing the excessive TiO₂ molar ratio. This result indicates the influential role of TiO₂-rich on the significantly improved dielectric properties of the NYCTO ceramics.
Figure 2. Dielectric properties at room temperature as a function of frequency for NYCTO + xTiO$_2$ ceramics with different doping content: (a) dielectric permittivity ($\varepsilon'$) and (b) loss tangent (tan$\delta$).

The temperature dependence of the dielectric properties of the NYCTO + xTiO$_2$ ceramics is illustrated in Figure 3a,b. In the temperature range from $-125$ to $110$ °C, the $\varepsilon'$ values of the NYCTO + 0.1TiO$_2$ and NYCTO + 0.2TiO$_2$ ceramics are more stable with temperature than that of the NYCTO ceramic. At the temperature below $-120$ °C, the $\varepsilon'$ rapidly decreased, corresponding to the rapid increase in tan$\delta$. This is the Maxwell—Wagner polarization relaxation in the NYCTO + xTiO$_2$ ceramics. Considering in the high-temperature range, the $\varepsilon'$ and tan$\delta$ significantly increase, which is associated with the DC conduction of free charge carriers associated with oxygen vacancies [11,33,51,52].
It is widely accepted that the colossal dielectric properties of the ACu$_3$Ti$_4$O$_{12}$ oxide groups is the result from the electrical heterogeneous in the microstructure [5,11,15,30,33,48]. The electrically heterogeneous microstructure can be confirmed using impedance spectroscopy [5,53]. Furthermore, the heterogeneous electrical microstructure can also be used to explain the nonlinear electrical properties of the ACu$_3$Ti$_4$O$_{12}$ compounds [21,23,24]. Generally, the semicircular arc due to the electrical response of the semiconducting grains of the ACu$_3$Ti$_4$O$_{12}$ compounds can be observed in the impedance complex plane (Z*) plots at low temperatures [5,54]. Thus, to confirm the formation of semiconducting grains, Z* plots of all the NYCTO + xTiO$_2$ ceramics are demonstrated at −100 °C, as shown in Figure 3c. The semicircular arcs of all the ceramics can be observed, while only parts of relatively large semicircular arcs can be observed. These two parts can be assigned as the electrical responses of the semiconducting grain and insulating GB, respectively [5,54].
The grain resistance ($R_g$), which can be calculated from the diameter of the semicircular arc of the NYCTO + xTiO$_2$ ceramics, was increased by increasing the TiO$_2$ molar ratio. In general, we expect that the TiO$_2$—rich should not affect the electrical properties of the semiconducting grains but should only affect the insulating boundaries due to the segregation of the TiO$_2$—rich phase. In this current study, the excessive TiO$_2$ molar ratio can affect the electrical properties inside the semiconducting grains, which will be discussed in the last section. Nevertheless, according to the impedance spectroscopy, the variation in the colossal dielectric properties and dielectric behavior of the NYCTO + xTiO$_2$ ceramics should be described in all aspects based on the IBLC model.

Figure 4a displays the $Z^*$ plots of all the ceramics at 30 °C. Only parts of the relatively large arcs can be observed with a nonzero intercept (inset of Figure 4a), which is similar to that reported in the previous works [5,6,12,19,21,44,54]. The $R_g$ value at 30 °C, which can be calculated from the nonzero intercept, increases with increasing the excessive TiO$_2$ molar ratio. Even though an entire arc cannot be observed, the $R_{gb}$ values of all the NYCTO + xTiO$_2$ ceramics can be estimated. As shown in Figure 4b, the tanδ of the NYCTO + xTiO$_2$ ceramics is inversely proportional to the $R_{gb}$ value. According to the IBLC structure [20,44], the low—frequency tanδ value is correlated to the total resistance, which is governed by the $R_{gb}$ value. The low—frequency tanδ can be reduced by increasing $R_{gb}$. Thus, the correlation of the tanδ and $R_{gb}$ values follows the IBLC model.

![Figure 4](image_url)  
Figure 4. (a) Impedance complex plane ($Z^*$) plots of NYCTO + xTiO$_2$ ceramics at 30 °C; inset shows the enlarged view near the origin, showing a nonzero intercept. (b) Relationship of loss tangent (tanδ) at 1 kHz and 30 °C and grain boundary resistance ($R_{gb}$) at 30 °C.
In addition to the variation in $\tan \phi$, the IBLC model should be used to reasonably describe the overall dielectric properties of the NYCTO + xTiO$_2$ ceramics. Therefore, the microstructure of the sintered ceramics was studied. Figure 5 shows the SEM images of the polished surface of the NYCTO + xTiO$_2$ ceramics and their grain size distributions. All the ceramics reveal the grain and GB structure with a highly dense microstructure. The mean grain size of the NYCTO + xTiO$_2$ ceramics was extremely reduced by increasing x from 0 to 0.2. This result is similar to that reported in the previous reports for TiO$_2$—rich CCTO ceramics [6]. The mean grain sizes of the NYCTO + xTiO$_2$ ceramics with $x = 0, 0.1$ and 0.2 are $32.80 \pm 20.44, 4.05 \pm 2.08$ and $3.18 \pm 1.35 \mu m$, respectively. The excessive TiO$_2$ could intercept the grain growth rate of the NYCTO ceramics due to the pinning effect of excessive TiO$_2$—rich phase particles during the sintering process [55]. We also found that the segregation of the Cu—rich phase is slightly observed along the grain boundaries, as remarked in the square area of Figure 5b.

![Figure 5. SEM images of NYCTO + xTiO$_2$ ceramics with $x = (a) 0.0, (b) 0.1$ and (c) 0.2 and grain size distributions of NYCTO + xTiO$_2$ ceramics with $x = (d) 0.0, (e) 0.1$ and (f) 0.2.](image)

The observed decrease in $\epsilon'$ (Figure 2a) value of the NYCTO + xTiO$_2$ ceramics should be caused by the decrease in the mean grain size, following a simple series layer model of the IBLC structure [20,44,56],

$$
\epsilon' = \frac{\epsilon'_{gb} G}{t_{gb}}
$$

where $G$ is the mean grain size, $t_{gb}$ is the thickness of the GB and $\epsilon'_{gb}$ is the dielectric constant of the GBs. Furthermore, it is also suggested that, but does not clearly prove, the decrease in the $\epsilon'$ might be due to the increase in $t_{gb}$ due to the TiO$_2$—rich phase. The EDS and ED—SEM mapping techniques were used to further characterize the microstructure and elemental distribution. As revealed in Figure 6a and its inset, all elements comprising the NYCTO + 0.1TiO$_2$ ceramic are observed in the EDS spectra, confirming the existence of Na, Y, Cu, Ti and O elements. As demonstrated in Figure 6b—g, the Na, Y, Cu and O elements disperse well throughout the microstructure. It is observed that the relatively higher brightness of Ti mapping element along the GBs compared to that of the grains can be observed, confirming the segregation of TiO$_2$—rich boundary. Thus, this is one of the most important factors contributing to the decrease in the $\epsilon'$ values of the NYCTO + 0.1TiO$_2$ and NYCTO + 0.2TiO$_2$ ceramics. According to the microstructure analyses, the density of the insulating GB layers in the NYCTO + xTiO$_2$ ceramics was significantly increased by
increasing TiO$_2$—rich phase owing to the decreased mean grain size [9,20]. Obviously, the significantly increased $R_{gb}$ (Figure 4) is also attributed to the enhancement of insulating GB density. Furthermore, the increased $R_{gb}$ is also due to the increase in $t_{gb}$. The XEX spectra detected at the grain and GB areas are shown in Figure 7. It was found that the percentage ratios of Ti(wt%)/Cu(wt%) at the grain and GB were found to be 0.808 and 0.834, respectively.

Figure 6. (a) EDS spectrum of NYCTO + xTiO$_2$ ceramic with $x = 0.1$; inset shows EDS testing area. (b) SEM image and corresponding SEM—EDS mapping images of (c) Na, (d) Y, (e) Cu, (f) Ti and (g) O for NYCTO + xTiO$_2$ ceramic with $x = 0.1$. 
Figure 7. EDX spectra of NYCTO + xTiO₂ ceramic with x = 0.2 detected at (a) grain and (b) GB; insets show the detected points in the microstructure.

According to our previous work [28,29], it was found that the NYCTO ceramics exhibited the nonlinear J–E characteristics with nonlinear coefficients (α) of 5.7–6.6. Furthermore, it was reported that the nonlinear properties of CCTO ceramics could be enhanced by increasing the excessive TiO₂ molar ratio [6,7]. The α value of the CaCu₃Ti₄+xO₁₂+2x ceramic with x = 0.15 was increased to 7.9. As illustrated in Figure 8, all the NYCTO + xTiO₂ ceramics exhibit the J–E characteristics. The α and electric breakdown (E_b) of the NYCTO, NYCTO + 0.1TiO₂ and NYCTO + 0.2TiO₂ ceramics are 4.96 and 724.50 V/cm, 4.71 and 910.59 V/cm, and 13.36 and 7948.04 V/cm, respectively. The E_b increased significantly with increasing TiO₂—rich phase, similar to that observed in the CaCu₃Ti₄+xO₁₂+2x ceramics [6]. Nevertheless, the enhanced α value of 13.36 is larger than that of the CaCu₃Ti₄+xO₁₂+2x ceramics. The segregation of TiO₂—rich boundary and the increased GB density are the key factors, giving rise to the significantly improved nonlinear J–E properties. The α value is often related to E_b value [4].
ary vacancies and/or oxygen enrichment at the GBs due to the segregation of TiO$_2$—rich boundary [7,18]. The increased $E_b$ value is associated with the increase in $R_{gb}$ due to the significantly increased GB density and GB thickness, which are classified as the geometric factors of the GBs [9]. Furthermore, the intrinsic factor of the GBs, i.e., the Schottky barrier height ($\Phi_b$), can usually have a remarkable effect on the $R_{gb}$ and $E_b$ values [4,5,7,9]. The $\Phi_b$ is closely related to the conduction activation energy at the GBs ($E_{gb}$) [7,13,14]. To calculate the $E_{gb}$ value, $R_{gb}$ values at different temperatures were calculated. Figure 9a and its inset show $Z^*$ plots and nonzero intercept of the NYCTO ceramic at various temperatures. The $R_b$ and $R_{gb}$ values can be obtained and found to decrease with increasing temperature. Thus, $E_{gb}$ can be calculated by using the Arrhenius law [5,9]:

$$R_{gb} = R_0 \exp \left( \frac{E_{gb}}{k_B T} \right),$$

where $R_0$, $k_B$ and $T$ are the per-exponential constant term, Boltzmann constant and absolute temperature, respectively. Figure 9b depicts the relationship between $R_{gb}$ and 1000/$T$ of the NYCTO + xTiO$_2$ ceramics. The $E_{gb}$ values can be calculated from the slopes of the $R_{gb}$ and 1000/$T$ plots, which are linearly fitted by using the Arrhenius law. The $E_{gb}$ values of the NYCTO + xTiO$_2$ ceramics are 0.547, 0.583 and 0.714 eV, respectively. Therefore, $\Phi_b$ of the NYCTO + xTiO$_2$ ceramics can be increased by increasing the TiO$_2$—rich phase. The improved nonlinear $J$–$E$ properties and electrical properties of the GBs are also caused by the enhanced $\Phi_b$, just as observed in the TiO$_2$—rich CCTO ceramics [7]. The increased $\Phi_b$ values of the NYCTO + xTiO$_2$ ceramics are likely attributed to the suppressed oxygen vacancies and/or oxygen enrichment at the GBs due to the segregation of TiO$_2$—rich boundary [7,18].

**Figure 8.** Nonlinear current density ($J$)—Electric field ($E$) at room temperature for NYCTO + xTiO$_2$ ceramics with $x = 0.0, 0.1$ and $0.2$. The nonlinear electrical behavior of ACu$_3$Ti$_4$O$_{12}$ oxides is widely believed to be originated by the formation of the Schottky barrier at the GBs [4,5,7,18]. The increased $E_b$ value is associated with the increase in $R_{gb}$ due to the significantly increased GB density and GB thickness, which are classified as the geometric factors of the GBs [9]. Furthermore, the intrinsic factor of the GBs, i.e., the Schottky barrier height ($\Phi_b$), can usually have a remarkable effect on the $R_{gb}$ and $E_b$ values [4,5,7,9]. The $\Phi_b$ is closely related to the conduction activation energy at the GBs ($E_{gb}$) [7,13,14]. To calculate the $E_{gb}$ value, $R_{gb}$ values at different temperatures were calculated. Figure 9a and its inset show $Z^*$ plots and nonzero intercept of the NYCTO ceramic at various temperatures. The $R_b$ and $R_{gb}$ values can be obtained and found to decrease with increasing temperature. Thus, $E_{gb}$ can be calculated by using the Arrhenius law [5,9]:

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Figure 9. (a) Impedance complex plane plots (Z*) of NYCTO ceramic at various temperature (140–210 °C). (b) Arrhenius plot for grain boundary conductivity (R_gb).

In addition to the electrical properties of the GBs, the electrical properties of the semiconducting grains must also be characterized. The conduction activation energy of the grains (E_g) can be calculated from the temperature dependence of R_g. The R_g values at a low-temperature range can be easily calculated using the admittance spectroscopy (Y*) [28,29,57], as the following equation:

\[
Y* = \frac{R_{gb}^{-1}}{1 - \omega^2 \tau_g \tau_{gb} + i \omega \tau_{gb}},
\]

where \( \tau_{gb} = R_{gb} C_{gb} \), \( \tau_g = R_g C_g \) and \( \tau = R_g C_{gb} \) and \( C_g \) and \( C_{gb} \) are the grain and GB capacitance values, respectively. According to the impedance spectroscopy, it was found that \( R_{gb} \gg R_g \) and \( C_{gb} \gg C_g \). From Equation (3), \( R_g \) can be obtained from the relation \( R_g^\prime = 1/Y_{max}'' \), where \( Y_{max}'' \) is the maximum value at \( Y'' \) peak. As shown in Figure 10a–c, \( Y_{max}'' \) appears in the temperature range from −60 to 0 °C. Consequently, \( E_g \) can be calculated by using the Arhenius law, \( \sigma_g = \sigma_0 \exp(-E_g/k_B T) \), where \( \sigma_g \) is the grain conductivity (\( \sigma_g \propto 1/R_g \)), and \( \sigma_0 \) is a per-exponential constant term. The \( E_g \) can be calculated by the linear fitting data, as demonstrated in the insets of Figure 10a–c. The \( E_g \) values are 0.112, 0.118 and
0.126 eV for the NYCTO, NYCTO + 0.1TiO\textsubscript{2} and NYCTO + 0.2TiO\textsubscript{2} ceramics, respectively. The $E_g$ slightly increased with increasing the excessive TiO\textsubscript{2}, corresponding to the increase in $R_g$ (Figure 3c). The difference between $E_g$ and $E_{gb}$ clearly indicates the formation of IBLC microstructure, consisting of the semiconducting grains and insulating GBs.

The XPS technique was further used to characterize the electrical properties of the grains. Figure 11a–c displays the XPS spectra of the Cu 2p\textsubscript{3/2} for the NYCTO, NYCTO + 0.1TiO\textsubscript{2} and NYCTO + 0.2TiO\textsubscript{2} ceramics, respectively. According to the fitted curves, the XPS peak of the Cu 2p\textsubscript{3/2} can be divided into two peaks at relatively low and high binding energies, corresponding to the Cu\textsuperscript{+} and Cu\textsuperscript{2+}, respectively. Note that only Ti\textsuperscript{4+} can be detected in the XPS spectra, as shown in Figure 11d–f. Thus, the conduction in the semiconducting grains of all the ceramics is attributed to the electron hopping between Cu\textsuperscript{+} $\leftrightarrow$ Cu\textsuperscript{2+}. The Cu\textsuperscript{+}/Cu\textsuperscript{2+} ratios of the NYCTO, NYCTO + 0.1TiO\textsubscript{2} and NYCTO + 0.2TiO\textsubscript{2} ceramics are 0.069 ± 0.027, 0.053 ± 0.021 and 0.049 ± 0.020, respectively. The Cu\textsuperscript{+}/Cu\textsuperscript{2+} ratios decreased
with increasing TiO$_2$—rich phase. Generally, CCTO and related ACu$_3$Ti$_4$O$_{12}$ ceramics lose a small amount of oxygen during sintering, giving rise to oxygen vacancies and associated free electrons [5,9]. Accordingly, a small amount of Cu$^+$ and/or Ti$^{4+}$ can be detected. For the NYCTO + 0.1TiO$_2$ and NYCTO + 0.2TiO$_2$ ceramics, the diffusion of oxygen vacancies during the sintering process may be inhibited by the segregation of TiO$_2$—rich phase along the GBs. Thus, the oxygen loss and related oxygen vacancies in the TiO$_2$—rich NYCTO ceramics were reduced, leading to the decrease in Cu$^+$ ions. The increased $R_g$ (Figure 3c) can be proved to be caused by the decreased Cu$^+/Cu^{2+}$ ratios. In addition to the grain size effect, the observed decrease in the $\varepsilon'$ of the NYCTO + 0.1TiO$_2$ and NYCTO + 0.2TiO$_2$ ceramics can be described based on the IBLC microstructure. Under an applied electric field, charge carriers inside the semiconducting grains are moved to trap at the insulating GB due to a high potential barrier height, inducing the interfacial polarization and hence high $\varepsilon'$ value. The intensity of the interfacial polarization of the NYCTO + 0.1TiO$_2$ and NYCTO + 0.2TiO$_2$ ceramics should be lower than that of the NYCTO ceramic because of a lower concentration of free carriers inside the grains, which is considered by a larger $R_g$ value.

![Figure 11](image-url)

**Figure 11.** (a–c) XPS spectra of Cu 2p$_{3/2}$ for all sintered NYCTO + xTiO$_2$ ceramics. (d–f) XPS spectra of Ti 2p for all sintered NYCTO + xTiO$_2$ ceramics.
4. Conclusions

In conclusion, we have successfully synthesized the TiO$_2$—rich NYCTO ceramics prepared using the SSR method. The effects of Ti—excess on the microstructure, colossal dielectric properties and nonlinear $J$—$E$ characteristics were studied. Only the main phase of the NYCTO structure was detected in the XRD patterns, which might be due to the presence of an amorphous phase of TiO$_2$ along the GBs. Significantly reduced grain with highly dense microstructure was observed in the TiO$_2$—rich NYCTO ceramics, which was due to the pinning effect of the TiO$_2$—rich phase particles. The reduced grain sizes, which can cause an increase in the GB density, resulted in the significant enhancement of $R_{gb}$, and hence reduced $\tan\delta$. The colossal $\varepsilon'$ values of $\sim 0.7$–$1.4 \times 10^4$ was achieved in the TiO$_2$—rich NYCTO ceramics. The TiO$_2$—rich NYCTO ceramics also showed the enhanced nonlinear $J$—$E$ properties due to the improved GB properties. The $R_g$ value was also increased owing to the decreased Cu$^+$/Cu$^{2+}$ ratio, confirming by the XPS result. The overall colossal dielectric permittivity and nonlinear electrical properties were well described using the Maxwell—Wagner polarization relaxation model based on the formation of the Schottky barrier at the grain boundary.

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