Magnetic field dependence of the oxygen isotope effect on the magnetic penetration depth in hole-doped cuprate superconductors

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The magnetic field dependence of the oxygen-isotope (\(^{16}\text{O}/^{18}\text{O}\)) effect (OIE) on the in-plane magnetic field penetration depth \(\lambda_{ab}\) was studied in the hole-doped high-temperature cuprate superconductors \(\text{YBa}_2\text{Cu}_4\text{O}_{8}\), \(\text{Y}_{0.8}\text{Pr}_{0.2}\text{Ba}_2\text{Cu}_3\text{O}_{7-\delta}\), and \(\text{Y}_{0.7}\text{Pr}_{0.3}\text{Ba}_2\text{Cu}_3\text{O}_{7-\delta}\). It was found that \(\lambda_{ab}\) for the \(^{16}\text{O}\) substituted samples increases stronger with increasing magnetic field than for the \(^{18}\text{O}\) ones. The OIE on \(\lambda_{ab}\) decreases by more than a factor of two with increasing magnetic field from \(\mu_0H = 0.2\) T to \(\mu_0H = 0.6\) T. This effect can be explained by the isotope dependence of the in-plane charge carrier mass \(m^*_{ab}\).

The density of the delocalized states was found to increase proportionally to \(\sqrt{H}\). The nonlinear correction to \(\lambda_{ab}\) arises from magnetic momenta on the Fermi surface close to the gap nodes. This is because the coherence length \(\xi\), being inversely proportional to the gap, becomes very large close to the nodes and formally diverges at the nodal points. Thus, there exist areas on the Fermi surface where \(\lambda/\xi \lesssim 1\), and the response of a superconductor to an applied magnetic field becomes nonlocal.

A simple analysis reveals that both the nonlinear and the nonlocal corrections depend on the supercarrier mass \(m^*\). Indeed, the nonlinear correction to \(\lambda_{ab}\) depends on the excitation energy \(\varepsilon\) [see Eq. (1)] and, therefore, will increase with increasing \(\varepsilon\). Bearing in mind that \(|\mathbf{v}_F| \propto 1/m^*\) and \(|\mathbf{v}_s| \propto 1/m^*\), the excitation energy is proportional to \(1/m^*\). Thus the nonlinear correction to \(\lambda_{ab}\) decreases with increasing supercarrier mass \(m^*\). On the other hand, the nonlocal correction depends on the Fermi surface area where, due to the growing of \(\xi\) close to the nodes, \(\lambda/\xi \lesssim 1\). Therefore, the nonlocal correction will decrease with increasing Ginzburg-Landau parameter \(\kappa = \lambda_{ab}/\xi\). Taking into account that within the simple London model \(\lambda \sim 2 \propto 1/m^*\) and \(\xi_0 \propto |\mathbf{v}_F|/\Delta_0\), one can easily get \(\kappa \propto (m^*)^{3/2}\) (\(\xi_0\) and \(\Delta_0\) are the mean values of the coherence length and the superconducting gap, respectively). This implies that the nonlocal correction to \(\lambda_{ab}\), in full analogy with the nonlinear one, decreases with increasing \(m^*\). As a consequence, the magnetic field dependence of \(\lambda_{ab}\) is expected to be stronger for a superconductor with a smaller \(m^*\).

A study of the field dependence of the isotope effect on \(\lambda_{ab}\) can serve as a direct test of this prediction. Indeed, several oxygen isotope (\(^{16}\text{O}/^{18}\text{O}\)) effect (OIE) studies of the in-plane penetration depth \(\lambda_{ab}\) in various cuprate families \(\text{Y}_{1-x}\text{Pr}_x\text{Ba}_2\text{Cu}_3\text{O}_{7-\delta}\), \(\text{YBa}_2\text{Cu}_4\text{O}_{8}\), \(\text{La}_{2-y}\text{Sr}_y\text{CuO}_4\), \(\text{Bi}_{1.6}\text{Pb}_{0.4}\text{Sr}_2\text{Ca}_2\text{Cu}_3\text{O}_{10+\delta}\), and \(\text{Pr}_{0.2}\text{Ba}_2\text{Cu}_3\text{O}_{7-\delta}\) showed a pronounced oxygen-mass dependence of the in-plane supercarrier mass with \(18m^*_{ab} > 16m^*_{ab}\). This implies that \(16\lambda_{ab}\) should increase stronger with magnetic field than \(18\lambda_{ab}\). Bearing in mind that \(18\lambda_{ab}\) is always larger than \(16\lambda_{ab}\), the OIE on \(\lambda_{ab}\)
[\Delta \lambda_{ab}/\lambda_{ab} = \left(^{18}\lambda_{ab}-^{16}\lambda_{ab}\right)/^{16}\lambda_{ab}]$ should decrease with increasing magnetic field (hereafter the indices 16 and 18 denote $^{16}$O and $^{18}$O substituted samples, respectively).

Here, we report a study of the magnetic field dependence of the OIE on $\lambda_{ab}$ in YBa$_2$Cu$_4$O$_8$ and Y$_{1-x}$Pr$_x$Ba$_2$Cu$_3$O$_{7-\delta}$ ($x = 0.2$, 0.3) by means of the muon-spin rotation ($\mu$SR) technique. The isotope shift of $\lambda_{ab}$ at $T = 0$ was found to decrease from $\Delta \lambda_{ab}/\lambda_{ab} = 2.2(6)\%$, 2.4(4)\%, and 2.1(6)\% at $\mu_0 H = 0.2$ T to 0.9(6)\%, 1.0(4)\%, and 0.9(6)\% at $\mu_0 H = 0.6$ T for YBa$_2$Cu$_4$O$_8$, Y$_{0.8}\text{Pr}_{0.2}$Ba$_2$Cu$_3$O$_{7-\delta}$, and Y$_{0.7}\text{Pr}_{0.3}$Ba$_2$Cu$_3$O$_{7-\delta}$, respectively. Moreover, measurements of the magnetic field dependence of $\lambda_{ab}$ at $T = 20$ K for YBa$_2$Cu$_4$O$_8$ reveal that for $\mu_0 H \geq 0.2$ T, the penetration depth $\lambda_{ab}$ increases stronger for the $^{16}$O substituted sample than for the $^{18}$O substituted one, consistent with the finding $^{18}m_{ab}^{*} > ^{16}m_{ab}^{*}$.

Details on the sample preparation for YBa$_2$Cu$_4$O$_8$ and Y$_{1-x}$Pr$_x$Ba$_2$Cu$_3$O$_{7-\delta}$ ($x = 0.2$, 0.3) can be found elsewhere. Oxygen isotope exchange was performed during heating the samples in $^{18}$O$_2$ gas. In order to ensure that the $^{16}$O and $^{18}$O substituted samples are the subject of the same thermal history, the annealing of the two samples was performed simultaneously in $^{16}$O$_2$ and $^{18}$O$_2$ (95% enriched) gas, respectively. The $^{18}$O content in all the samples, as determined from a change of the sample weight after the isotope exchange, was found to be $82(2)\%$.

The transverse-field $\mu$SR experiments were performed at the Paul Scherrer Institute (PSI), Switzerland, using the $\pi$M3 $\mu$SR facility. In a powder sample the magnetic penetration depth $\lambda$ can be extracted from the muon-spin depolarization rate $\sigma(T) \propto 1/\lambda^2(T)$, which probes the second moment $\langle \Delta B^2 \rangle$ of the probability distribution of the local magnetic field function $p(B)$ in the mixed state. For highly anisotropic layered superconductors (like cuprate superconductors) $\lambda$ is mainly determined by the in-plane penetration depth $\lambda_{ab}$: $\sigma(T) \propto 1/\lambda_{ab}^2(T)$. The depolarization rate $\sigma$ was extracted from the $\mu$SR time spectra using a Gaussian re-
laxation function $R(t) = \exp[-\sigma^2t^2/2]$. The superconducting contribution $\sigma_{sc}$ was then obtained by subtracting the dipolar contribution $\sigma_{nm}$ measured above $T_c$ as $\sigma^2 = \sigma_{sc}^2 - \sigma_{nm}^2$.

Fig. 1 shows the temperature dependences of $\sigma_{sc}$ for the samples studied in this work, measured after field-cooling the samples from far above $T_c$ in $\mu_0 H = 0.2$ T (a) and 0.6 T (b). In both fields $\sigma_{sc}$ for the $^{16}$O substituted samples is systematically lower than those for the $^{18}$O substituted samples. The data in Fig. 1 were fitted with the power law $\sigma_{sc}(T)/\sigma_{sc}(0) = 1 - (T/T_c)^{n}$ \cite{21} with $\sigma_{sc}(0)$, $n$, and $T_c$ as free parameters. The values of $T_c$ and $\sigma_{sc}(0)$, obtained from the fits are listed in Table I. From $\sigma_{sc}(0)$ the relative isotope shift of the in-plane penetration depth $\Delta \lambda_{ab}(0)/\lambda_{ab}(0) = -0.5 \cdot \frac{[^{18}\sigma_{sc}(0) - ^{16}\sigma_{sc}(0)]}{^{16}\sigma_{sc}(0)}$ was determined (see Table I). The values of $\Delta \lambda_{ab}(0)/\lambda_{ab}(0)$ were corrected for the incomplete $^{18}$O content (82%) of the $^{18}$O substituted samples.

Two important points should be considered: (i) For all the samples (except $^{18}$O substituted Y$_{0.7}$Pr$_{0.3}$Ba$_2$Cu$_2$O$_{7-\delta}$) $\sigma_{sc}(0)$ decreases with increasing magnetic field. The changes of $\sigma_{sc}(0)$ for both oxygen isotopes were found to be $|\sigma_{sc}(0.6T) - \sigma_{sc}(0.2T)|/\sigma_{sc}(0.2T) \approx -5\%$, $\approx -6\%$, and $\approx -1\%$ for YBa$_2$Cu$_2$O$_8$, Y$_{0.8}$Pr$_{0.2}$Ba$_2$Cu$_2$O$_{7-\delta}$, and Y$_{0.7}$Pr$_{0.3}$Ba$_2$Cu$_2$O$_{7-\delta}$, respectively. Note, that the values for YBa$_2$Cu$_2$O$_8$ and Y$_{0.8}$Pr$_{0.2}$Ba$_2$Cu$_2$O$_{7-\delta}$ are in fair agreement with those reported in the literature for optimally doped YBa$_2$Cu$_2$O$_8$ and La$_{1.85}$Sr$_{0.15}$CuO$_4$ \cite{23}. The value of $-1\%$ obtained for Y$_{0.7}$Pr$_{0.3}$Ba$_2$Cu$_2$O$_{7-\delta}$ is somehow small. The reason for that is probably the enhancement of the magnetic contribution to the muon relaxation rate $\sigma$ at higher fields, observed in similar samples below $\sim 10$ K \cite{24}. (ii) In both fields $^{16}\sigma_{sc}(0) > ^{18}\sigma_{sc}(0) > ^{18}\lambda_{ab}(0)$, $^{16}\lambda_{ab}(0) < ^{18}\lambda_{ab}(0)$, implying that the in-plane charge carriers are heavier in the $^{18}$O substituted samples than in the $^{16}$O substituted ones, as it was previously observed for various HTS \cite{25,26,27,28,29,30,31,32,33,34,35,36,37,38,39,40,41,42,43,44,45,46,47,48,49}. For all the samples the oxygen isotope shift $\Delta \lambda_{ab}(0)/\lambda_{ab}(0)$ decreases by more than a factor of two with increasing the magnetic field from 0.2 T to 0.6 T (see Table I). This implies that $^{16}\lambda_{ab}(0)$ increases stronger with field than $^{18}\lambda_{ab}(0)$, as expected for $^{16}m_{ab}^* > ^{18}m_{ab}^*$ (see above).

I order to study the magnetic field dependence of $\lambda_{ab}$ in more detail, $\sigma_{sc}$ was measured as a function of $H$ at $T = 20$ K for the $^{16}$O and $^{18}$O substituted YBa$_2$Cu$_2$O$_8$ samples (see Fig. 2). For both samples $\sigma_{sc}$ first increases, goes through a pronounced maximum around $\mu_0 H \sim 0.2$ T and than decreases. Note, that for conventional $s$–wave superconductors, where $\lambda$ is field independent, $\sigma_{sc}$ increases with increasing magnetic field up to $H \approx 2H_c1$ and then stays constant for fields much smaller than $H_c2$ \cite{22} ($H_{c1}$ and $H_{c2}$ are the first and the second critical fields, respectively). For $d$–wave superconductors, however, $\lambda$ depends on the field. This leads to a decrease of $\sigma_{sc}(H)$ for magnetic fields higher that $2H_c1$. Such behavior is generally observed for various HTS \cite{3,21}. The solid lines represent results of the fits by means of the relation

$$\frac{\lambda_{ab}^{-2}(B)}{\lambda_{ab}^{-2}(B = 0)} = \frac{\sigma_{sc}(B)}{\sigma_{sc}(B = 0)} = 1 - K \cdot \sqrt{B},$$

(2)

which takes into account the nonlinear correction to $\lambda_{ab}$ \cite{25,26}. Here $K$ is the parameter depending on the strength of the nonlinear effect. In the analysis only the points above 0.1 T were considered. The magnetic field inside the sample was assumed to be equal to the external magnetic field $B \approx \mu_0 H_{ext}$. The fits yield: $^{16}\sigma_{sc}(B = 0) = 3.25(3) \mu s^{-1}$, $^{16}K = 0.282(5) T^{-1/2}$, and $^{18}\sigma_{sc}(B = 0) = 3.02(3) \mu s^{-1}$, $^{18}K = 0.220(5) T^{-1/2}$ for the $^{16}$O and $^{18}$O substituted samples, respectively. The larger $^{16}\sigma_{sc}(B)$ and its stronger field decrease in comparison with $^{18}\sigma_{sc}(B)$ is consistent with the finding $^{16}m_{ab}^* > ^{18}m_{ab}^*$ \cite{8,9,11,12,13,14,15,16,17,18,19,20,21,22,23,24,25,26,27,28,29,30,31,32,33,34,35,36,37,38,39,40,41,42,43,44,45,46,47,48,49} and with the statement that the nonlinear and the nonlocal corrections to $\lambda_{ab}$ decrease with increasing in-plane supercarrier mass $m_{ab}^*$. One should mention, however, that the measurements were performed in magnetic fields well below $H_{c2}$ ($0.0006 \leq H/H_{c2} \leq 0.008$), so that it is difficult to draw any firm conclusion about the precise field dependence of $\lambda_{ab}$. In particular, the stronger field dependence of $^{16}\sigma_{sc}$ suggests that at some characteristic

![FIG. 2: (Color online) Magnetic field dependence of the $\mu$SR depolarization rate $\sigma_{sc}$ for $^{16}$O (○) and $^{18}$O (●) substituted YBa$_2$Cu$_2$O$_8$ samples at $T = 20$ K. Solid curves represent fits of the data using Eq. (2) (see text for details).](image-url)
field the sign of the OIE on \( \lambda_{ab} \) should change. Further investigations at higher fields are needed to clarify this point.

All the above observed features are consistent with the picture where the mass of the charge carriers \( m_{ab}^* \) depends on the oxygen isotope mass. It stems from the isotope dependence of the in-plane charge carrier mass above mentioned effects can be explained by the isotope dependence of the in-plane magnetic penetration depth \( \lambda_{ab} \), that was found to be larger for the samples with the heavier oxygen isotope \( ^{18}\lambda_{ab} > ^{16}\lambda_{ab} \). An additional confirmation comes from the stronger magnetic field dependence of \( \lambda_{ab} \) in the \(^{16}\)O substituted samples. The later one is determined by the fact that both the nonlinear and the nonlocal corrections to \( \lambda_{ab} \), arising from the presence of nodes in the superconducting gap, decrease with increasing \( m_{ab}^* \).

In conclusion, the magnetic field dependence of the OIE on the in-plane magnetic field penetration depth \( \lambda_{ab} \) was studied in \( \text{YBa}_2\text{Cu}_4\text{O}_8 \), \( \text{Y}_{0.8}\text{Pr}_{0.2}\text{Ba}_2\text{Cu}_3\text{O}_{7-\delta} \), and \( \text{Y}_{0.7}\text{Pr}_{0.3}\text{Ba}_2\text{Cu}_3\text{O}_{7-\delta} \) hole-doped HTS. As a result \( \lambda_{ab} \) for the \(^{16}\)O substituted samples increases stronger with magnetic field than for the \(^{18}\)O substituted ones. The OIE on \( \lambda_{ab} \) was found to decrease from \( \Delta\lambda_{ab}(0)/\lambda_{ab}(0) = 2.2(6)\% \), \( 2.4(4)\% \), and \( 2.1(6)\% \) at \( \mu_0H = 0.2 \text{T} \) to 0.9(6)\%, 1.0(4)\%, and 0.9(6)\% at \( \mu_0H = 0.6 \text{T} \) for \( \text{YBa}_2\text{Cu}_4\text{O}_8 \), \( \text{Y}_{0.8}\text{Pr}_{0.2}\text{Ba}_2\text{Cu}_3\text{O}_{7-\delta} \), and \( \text{Y}_{0.7}\text{Pr}_{0.3}\text{Ba}_2\text{Cu}_3\text{O}_{7-\delta} \), respectively. Both of the above mentioned effects can be explained by the isotope dependence of the in-plane charge carrier mass \( m_{ab}^* \).

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\begin{table}
\centering
\begin{tabular}{|c|c|c|c|c|c|c|c|c|c|}
\hline
Sample & \( ^{16}T_c \) & \( ^{16}\sigma_{sc}(0) \) & \( ^{18}T_c \) & \( ^{18}\sigma_{sc}(0) \) & \( \Delta\lambda_{ab}(0) \) & \( ^{16}T_c \) & \( ^{16}\sigma_{sc}(0) \) & \( ^{18}T_c \) & \( ^{18}\sigma_{sc}(0) \) & \( \Delta\lambda_{ab}(0) \) \\
 & [K] & [\mu s^{-1}] & [K] & [\mu s^{-1}] & [%] & [K] & [\mu s^{-1}] & [K] & [\mu s^{-1}] & [%] \\
\hline
\text{YBa}_2\text{Cu}_4\text{O}_8 & 81.03(65) & 3.06(2) & 79.77(45) & 2.95(2) & 2.2(6) & 80.17(37) & 2.86(2) & 79.99(37) & 2.82(2) & 0.9(6) \\
\text{Y}_{0.8}\text{Pr}_{0.2}\text{Ba}_2\text{Cu}_3\text{O}_{7-\delta} & 72.22(38) & 2.05(1) & 71.82(44) & 1.97(1) & 2.4(4) & 73.19(35) & 1.89(1) & 72.84(34) & 1.86(1) & 1.0(4) \\
\text{Y}_{0.7}\text{Pr}_{0.3}\text{Ba}_2\text{Cu}_3\text{O}_{7-\delta} & 57.05(57) & 1.45(1) & 55.23(34) & 1.40(1) & 2.1(6) & 56.88(39) & 1.42(1) & 56.21(31) & 1.40(1) & 0.9(6) \\
\hline
\end{tabular}
\caption{Summary of the OIE results for \( \text{YBa}_2\text{Cu}_4\text{O}_8 \), \( \text{Y}_{0.8}\text{Pr}_{0.2}\text{Ba}_2\text{Cu}_3\text{O}_{7-\delta} \), and \( \text{Y}_{0.7}\text{Pr}_{0.3}\text{Ba}_2\text{Cu}_3\text{O}_{7-\delta} \) extracted from the experimental data (see text for an explanation). The values of \( \Delta\lambda_{ab}(0)/\lambda_{ab}(0, H) \) were corrected for incomplete \(^{18}\)O exchange of 82\%.}
\end{table}

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