The kHz QPOs as a probe of the X-ray color–color diagram and accretion-disk structure for the atoll source 4U 1728-34

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ABSTRACT

We have taken the kHz QPOs as a tool to probe the correlation between the tracks of X-ray color–color diagram (CCD) and magnetosphere-disk positions for the atoll source 4U 1728-34, based on the assumptions that the upper kHz QPO is ascribed to the Keplerian orbital motion and the neutron star (NS) magnetosphere is defined by the dipole magnetic field. We find that from the island to the banana state, the inner accretion disk gradually approaches the NS surface with the radius decreasing from \( r \sim 33.0 \) km to \( r \sim 15.9 \) km, corresponding to the magnetic field from \( B(r) \sim 4.8 \times 10^9 \) G to \( B(r) \sim 4.3 \times 10^7 \) G. In addition, we note the characteristics of some particular radii of magnetosphere-disk \( r \) are: firstly, the whole atoll shape of the CCD links the disk radius range of \( r \sim 15.9-33.0 \) km, which is just located inside the corotation radius of \( 4U 1728-34 \) \( r_{\text{co}} \sim (34.4 \text{ km}) \), implying that the CCD shape is involved in the NS spin-up state. Secondly, the island and banana states of CCD correspond to the two particular boundaries: (I) near the corotation radius at \( r \sim 27.2-33.0 \) km, where the source lies in the island state; (II) near the NS surface at \( r \sim 15.9-22.3 \) km, where the source lies in both the island and banana states. Thirdly, the vertex of the atoll shape in CCD, where the radiation transition from the hard to soft photons occurs, is found to be near the NS surface at \( r \sim 16.4 \) km. The above results suggest that both the magnetic field and accretion environment are related to the CCD structure of atoll track, where the corotation radius and NS hard surface play the significant roles in the radiation distribution of atoll source.

Key words. X-rays: binaries – stars: neutron – stars: individual: 4U 1728-34 – accretion, accretion disks

1. Introduction

Neutron star low mass X-ray binaries (NS-LMXBs) can be classified as atoll and Z sources (Hasinger & van der Klis 1989; van der Klis et al. 2006) according to the patterns they trace out in the X-ray color–color diagrams (CCDs). From the top to bottom in CCD, the tracks of Z sources are called the horizontal, normal, and flare branches, while for atoll sources, they are called the extreme island, island, lower banana, and upper banana states. Initially, it is assumed that the mass-accretion rate of Z sources may increase monotonically along the branches (Hasinger 1990; Hasinger et al. 1990). However, this scenario cannot be used to interpret the “parallel tracks” phenomenon, in other words, the similar temporal and spectral properties are observed at the different luminosity (Méndez et al. 1999; Ford et al. 2000; van der Klis 2001). Alternatively, van der Klis (2001) proposed that the changes in the averaged accretion rate through the disk could be responsible for the motion along the Z track. In addition, the transition between the atoll and Z tracks has been observed in XTE J1701-462, which is explained as the influence by the changes in the accretion rate (Homan et al. 2007, 2010; Lin et al. 2009; Fridriksson et al. 2015). Other physical effects, for example, the NS magnetic field (Hasinger & van der Klis 1989), have been proposed to interpret the difference between the two-subclass sources, however, there is no consensus as to their origin.

In both the atoll and Z sources the twin kilohertz quasi-periodic oscillations (kHz QPOs, with lower \( f_1 \) and upper \( f_2 \)) have been detected by \textit{Rossi} X-ray Timing Explorer (RXTE; van der Klis et al. 2006), which show a non-linear relation between \( f_1 \) and \( f_2 \) (Belloni et al. 2002, 2005, 2007; Zhang et al. 2006) in the frequency range of \( \sim 100-1300 \) Hz (Wang et al. 2014). The frequencies of kHz QPOs are found to be correlated with other temporal and spectral features (e.g., Ford & van der Klis 1998; Kaaret et al. 1998; Psaltis et al. 1999; Belloni et al. 2002; Méndez 2006), and they often increase monotonically along both the atoll tracks (e.g., van Straaten et al. 2000, 2003; Altamirano et al. 2008) and Z tracks (e.g., Wijnands et al. 1997, 1998; Homan et al. 2002; Jonker et al. 2002; Lin et al. 2012). It is suggested that kHz QPOs may reflect the orbital motion of the accreting matter at the inner accretion disk (Kluźniak et al. 1990; van der Klis 2000 and references therein; Zhang & Wang 2013), which can be exploited to explore the physical environments in the strong gravitational field and strong magnetic field regions (Kluźniak et al. 1990; Abramowicz et al. 2003; Miller & Miller 2015). Wang et al. (2015, 2017) analyzed the relations of the kHz QPO emission radii with the NS radius and corotation radius, suggesting that the emission of kHz QPOs may be affected by the NS hard surface and the spin-up environment near the corotation radius.

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As yet, we do not understand why some atoll sources have been detected with the millisecond spin signals but the Z sources have not. In addition, among ~30 NS-LMXBs with detected NS spin signals (Burderi & Di Salvo 2013; van der Klis 2016), 12 sources have also been detected with twin kHz QPOs (Wang et al. 2017, 2018), including ten atoll sources. Particularly, in the atoll source 4U 1728-34 the X-ray burst oscillation has been observed with the frequency of 363 Hz (Strohmayer et al. 1996; Zhang et al. 2016), while it has also shown temporal variabilities on all timescales including kHz QPOs (e.g., Méndez & van der Klis 1999; Di Salvo et al. 2001; van Straaten et al. 2002; Mukherjee & Bhattacharyya 2012) and spectral evolution (e.g., Tarana et al. 2011; Mondal et al. 2017). The goal of this paper is to take the kHz QPOs as the tool to probe the relation between the X-ray CCD tracks of 4U 1728-34 and the magnetosphere-disk positions, and further investigate the effects of accretion environment and NS magnetic field on the formation of the atoll track.

The paper is organized as follows: In Sect. 2, we introduce the data of twin kHz QPOs and NS spin of 4U 1728-34. In Sect. 3 we probe the magnetosphere-disk positions and magnetic field strength along the atoll track. We have investigated the relation between the CCD shape and the particular disk radii, for example, NS radius and its corotation radius. In Sect. 4 we present the discussions and conclusions.

2. Parameters of 4U 1728-34

We collected the kHz QPO frequencies of 4U 1728-34 detected by Di Salvo et al. (2001) and the NS spin frequency detected by Strohmayer et al. (1996). For the kHz QPOs, Di Salvo et al. (2001) analyzed the RXTE data of 4U 1728-34 in 1996 between February 15 and March 1, 1996 on May 3, and 1997 between September 23 and October 1, with a total observation time of ~456 ks. The authors plot the CCD by defining the soft and hard colors in CCD as the ratio of the count rates in the bands 3.5–6.4 keV/2.0–3.5 keV and 9.7–16 keV/6.4–9.7 keV, respectively (see Fig. 1 in which we reproduce the CCD with the same dataset of RXTE used by Di Salvo et al. 2001). Then they divided the CCD into 19 intervals by the boxes as shown in Fig. 1 (see also Di Salvo et al. 2001), and further computed a power spectrum for each interval and fit the QPOs. The kHz QPOs have been detected in the intervals from [1] to [17] with the range of \( v_1 \sim 511–876.1 \) Hz and \( v_2 \sim 387–1158 \) Hz (see Table 1), where it can be seen that \( v_2 \) increases monotonically along the atoll track from the interval [1] to [17]. According to Di Salvo et al. (2001), the power spectra of interval [1]–[11] are typical of the island state of atoll sources, while the intervals [14]–[19] correspond to the lower and upper banana state, respectively. For the NS spin, Strohmayer et al. (1996) detected the burst oscillation of 4U 1728-34 with the frequency of 363 Hz during the type I X-ray burst (see Table 1), which can be inferred as the NS spin frequency (Boutloukos & Lamb 2008).

3. Characteristic radii and magnetic field strength

It is generally thought that the kHz QPOs reflect the motion of the accreting matter at the inner disk boundary around NS (Kluźniak et al. 1990; van der Klis 2000; van der Klis et al. 2006 and references therein). This implies the emission radius of the kHz QPOs may indicate the magnetosphere-disk radius. Furthermore, the kHz QPOs and color parameters at the different intervals in Fig. 1 are calculated by the same light curves (see Di Salvo et al. 2001 for the details), so the magnetosphere-disk structures at various positions in X-ray CCD can be approximately inferred by the emission radius of kHz QPOs. In this paper, we take the detected kHz QPOs (Di Salvo et al. 2001) and NS spin (Strohmayer et al. 1996) of 4U 1728-34 to investigate the evolution of its magnetosphere-disk structure along the atoll track based on some assumptions (see the following equations), including the Keplerian orbital motion and magnetic dipole field.

3.1. Magnetosphere-disk radius inferred by kHz QPOs

Usually, the upper kHz QPO frequency \( v_2 \) is assumed as the Keplerian orbital frequency \( v_K \) of the accretion plasma. The emission radius of the kHz QPOs is explained as the magnetosphere-disk radius (e.g., Miller et al. 1998; Stella & Vietri 1999; Stella et al. 1999; Lamb & Miller 2001; Zhang 2004):

\[
v_2 = v_K = \sqrt{\frac{GM}{4\pi^2 r^3}}, \tag{1}
\]

where \( G \) is the gravitational constant, \( M \) is the NS mass and \( r \) is the emission radius of the kHz QPOs referring to the NS center, that is, the magnetosphere-disk radius. By solving Eq. (1), \( r \) can be derived as

\[
r \approx \frac{(GM)}{4\pi^2} v_2^{2/3} \left(\frac{M}{1.6 M_\odot}\right)^{1/3} \left(\frac{v_2}{900 \text{Hz}}\right)^{-2/3}. \tag{2}
\]

We infer the magnetosphere-disk radius \( r \) by Eq. (2) with the detected \( v_2 \) values in Table 1 and the assumed NS mass of \( M \sim 1.6 M_\odot \) (on the average mass of the millisecond pulsars, see Zhang et al. 2011 and Özel & Freire 2016). The results are...
shown in Table 1, where it is noticed that \( r \sim \) with the assumed NS surface magnetic field strength \( B \sim \) by a factor of \( M \) inferred by Eq. (2) with the assumed NS mass \( M \sim 6 \) \( 10^6 \) G and NS radius \( R \sim 2 \) km. For clarity, the schematic diagram of the magnetosphere-disk structures corresponding to the internal \([1]–[17]\) in Fig. 2a, dominated gradually to the soft photons dominated. For clarity, Fig. 3 shows the schematic diagram of the magnetosphere-disk structures corresponding to the internal \([1]–[17]\) in Fig. 2a, where the \(-5\) km gap of the magnetosphere-disk radius between the internal \([6] \sim 27.2\) km and \([7] \sim 22.3\) km is obviously noticed.

### 3.2. Magnetic field strength at the magnetosphere-disk radius

In this paper the magnetic field of NS is assumed to be dipolar (Bhattacharya & van den Heuvel 1991):

\[
B(r) = B_s \left( \frac{R}{r} \right)^3 \sim r^{-3},
\]

where \( r \) is the radial distance referring to the NS center, \( B_s \) and \( R \) are the surface magnetic field strength and the stellar radius of NS, respectively.

We inferred the magnetic field strength at the magnetosphere-disk radius, i.e., \( B(r) \), by Eq. (3) with the inferred emission radius of kHz QPOs in Table 1, as well as with the assumed NS surface magnetic field strength \( B_s \sim 10^8 \) G (Zhang & Kojima 2006; Harding 2013; Mondal et al. 2017) and NS radius \( R \sim 12 \) km (Shaposhnikov et al. 2003; Miller & Miller 2015). The results are shown in Table 1, where \( B(r) \) ranges at \(-4.8 \times 10^6 \) G\(-4.3 \times 10^6 \) G, and it increases monotonically from the internal \([1] \sim 4.8 \times 10^6 \) G to interval \([17] \sim 4.3 \times 10^7 \) G, by nearly one order of magnitude.

### 3.3. Corotation radius

The corotation radius \( r_{co} \) in NS-LMXB is the radial distance referring to the NS center where the accretion plasma corotates with the NS magnetosphere, meaning that the Keplerian orbital frequency \( \nu_k \) there equals the NS spin frequency \( \nu_s \) (Bhattacharya & van den Heuvel 1991). Setting \( \nu_k = \nu_s \) in Eq. (1), \( r_{co} \) can be derived as

\[
r_{co} \approx \left( \frac{GM}{4\pi^2} \right)^{1/3} \nu_s^{-2/3} = 34.4(\text{km}) \left( \frac{M}{1.6M_\odot} \right)^{1/3} \left( \frac{\nu_s}{363 \text{ Hz}} \right)^{-2/3}.
\]
We infer the corotation radius of 4U 1728-34 by Eq. (4) with the inferred NS spin frequency of $\nu_s \sim 363$ Hz (Strohmayer et al. 1996) and the assumed NS mass of $M \sim 1.6 M_\odot$ (Zhang et al. 2011; Özel & Freire 2016), and obtain $r_{co} \sim 34.4$ km (see Table 1). We note that all the magnetosphere-disk radii ($r \sim 15.9$–33.0 km, see Table 1) of the source inferred by the kHz QPOs are smaller than its corotation radius (see also Fig. 3).

4. Discussions and conclusions

We assumed that the upper kHz QPO is ascribed to the Keplerian orbital motion and the NS magnetosphere is defined by the dipole magnetic field, as well as the detected kHz QPOs from Di Salvo et al. (2001) and NS spin (363 Hz) inferred by the type I X-ray burst oscillation (Strohmayer et al. 1996). Based on these assumptions, we investigated the evolution of the magnetosphere-disk structure of 4U 1728-34 along the atoll track. We find that the magnetosphere-disk radius of the source decreases monotonically from the island state to the banana state in CCD of the source. Below we summarize the details of the discussions and conclusions.

As the source evolves from the island state to the banana state, its magnetosphere-disk radius decreases nearly by half (see Table 1 and Fig. 2a), while the accretion disk gradually enters the stronger magnetic field region with the strength increasing by a factor of 9 (see Table 1 and Fig. 2b). We note that these results rely on the simplistic assumptions of the Keplerian motion and magnetic dipole field (see Eqs. (1)–(4)). However, the reality of the problem is much more complex: due to the viscous of the accretion plasma and its interaction with the NS magnetic field, the orbital velocity of the plasma at a certain radius may be less than the Keplerian orbital velocity there, and Eq. (1) should be revised as

$$v_2 = \xi \nu_K = \xi \sqrt{\frac{GM}{4\pi r^3}},$$

where $0 < \xi \leq 1$. The value of $\xi$ can be estimated as follows: the observed maximal kHz QPO frequency of 4U 1728-34 is $\sim 1200$ Hz (Migliari et al. 2003), inferring the Keplerian orbital radius of $r \sim 15.5$ km with the assumed NS mass of $1.6 M_\odot$. By assuming the actual emission radius should be less than 15.5 km, for example, $r \sim 15$ km, we can infer the value of $\xi$ to be

$$\xi = 95\% \left( \frac{v_2}{1200 \text{ Hz}} \right) \left( \frac{M}{1.6 M_\odot} \right)^{-1/2} \left( \frac{r}{15 \text{ km}} \right)^{3/2}.$$ 

If $\xi$ is a constant, the variation of the magnetosphere-disk radius from the internal [1] to [17] can be derived as $r_{[1]} / r_{[17]} \propto (v_{2[1]} / v_{2[17]})^{-2/3} \sim (387/1158)^{-2/3} \approx 2.1$. Furthermore, in vacuum, the dipole field lines are poloidal with $B \propto r^{-3}$, which
increases from the internal [1] to [17] by a factor of $B_{[17]}/B_{[1]} \propto (r_{[1]}/r_{[17]})^{3/5} \sim (2.1)^{3/5} \approx 9.2$. In the presence of the accretion disk, the field lines are initially "frozen-in" to the orbiting plasma, which hence are sheared in the $\phi$ direction (Ghosh & Lamb 1978; Shapiro & Teukolsky 1983). This shearing generates a sizeable $B_0$ component, causing the magnetic field strength around the accretion disk may be stronger than the dipole field, as a general form,

$$B(r) = B_0 \left( \frac{r}{r_c} \right)^{\alpha} ,$$

with $\alpha \geq 3$. If we assume $\alpha \sim 3.5$, the magnetic field strength from the internal [1] to [17] should increase by a factor of $B_{[17]}/B_{[1]} \propto (r_{[1]}/r_{[17]})^{3/5} \sim (2.1)^{3/5} \sim 13.4$. However, these corrections do not obviously affect the conclusions that, as the evolution of the atoll track of 4U 1728-34, the accretion disk moves toward the NS surface and gradually enters the stronger magnetic field region.

It can be seen from Fig. 2a that the whole atoll track of 4U 1728-34 is formed when the magnetosphere-disk radii are smaller than the corotation radius, i.e., $r/r_{co} \propto (r/\varphi V)^{2/3} \lesssim (363 \text{ Hz}/387 \text{ Hz})^{1/3} \sim 0.95$. The accretion plasma corotates with the magnetosphere at $r_{co}$, while according to the expression of the Keplerian orbital velocity:

$$v = \left( 2 \pi GM \nu_2 \right)^{1/3} \propto \varphi V^{1/3},$$

as the accretion disk moves toward the NS surface from the internal [1] to [17], the orbital velocity of the plasma increases gradually by a factor of $(1158^{1/3} - 3871/3)/3871^{1/3} \sim 44\%$. The large velocity difference $\Delta \varphi \propto \varphi V^{1/3} - \varphi V^{1/3}$ between the magnetosphere and the accretion disk may induce the strong interaction and release huge energy (Ford et al. 1998). We suspect that this process can provide the particular physical environment to soften the photons, which causes the evolution of the atoll track from island state to banana state.

Figure 3 shows a position gap around $r \sim 27.2-22.3$ km between the internal [6] and [7] (see Table 1), which can be used to classify the magnetosphere-disk structures into two categories: (I)internal [1]–[6] with $r \sim 27.2-33.0$ km, where the source is in the island state and $r$ is near the corotation radius ($r_{co} \sim 34.4$ km, see Table 1); (II)internal [7]–[17] with $r \sim 15.9-22.3$ km, where the source is in the island state and banana state with $r$ approaching the NS surface. This "gap" may be due to the lack of the observational time (Zhang et al. 2016). However, we also suggest that the corotation radius and NS surface may be the two characteristic boundaries for the atoll track evolution: the corotation radius may be a soft boundary, and we may be the two characteristic boundaries for the atoll track evolution. In other words, $M_{\text{rad}}$ can modulate both the luminosity and the colors of the source, which modulates a same magnetosphere-disk radius as a $M_d$ does, thus a phenomenon of the parallel tracks occurs.

Based on the above discussions, we suggest that the atoll track in CCD of 4U 1728-34 may correspond to the particular magnetosphere-disk boundary, where the corotation radius and NS hard surface could play a significant role in the different radiation processes. In addition, it seems that the magnetic field strength and spin-up state of NS may also contribute to the radiation composition in the CCD. As a further exploration, however, similar investigations in other atoll sources and Z sources are needed to test whether these phenomena are common to all NS-LMXBs. If confirmed, these results will help to understand the formation mechanism of the atoll CCD track, to probe the accretion environment, and the magnet field structure around NS, and also to test the presence mechanism of kHz QPOs.

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The parallel tracks in the kHz QPO evolution have been observed in 4U 1728-34 (Méndez et al. 2001; van der Klis 2001), in other words, the same kHz QPO frequency could correspond to at least two different luminosities (or count rates) and colors during different observations. This phenomenon may deviate from our conclusion, since taking a different track may end up with different results for the same frequency. Here we have adopted the double accretion rates suggested by van der Klis (2001) to explain this phenomenon of parallel lines. As such, the luminosity of the source depends on the total mass accretion rate $M_{\text{tot}}$, which comes from the disk accretion $M_d$ and the radial accretion $M_{\text{rad}}$ (see also Pan et al. 2016):

$$M_{\text{tot}} = M_d + M_{\text{rad}}.$$
