AN APPARENT REDSHIFT DEPENDENCE OF QUASAR CONTINUUM: IMPLICATION FOR COSMIC DUST EXTINCTION?

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ABSTRACT

We investigate the luminosity and redshift dependence of the quasar continuum by means of the composite spectrum using a large non-BAL radio-quiet quasar sample drawn from the Sloan Digital Sky Survey. Quasar continuum slopes in the UV-Opt band are measured at two different wavelength ranges, i.e., $\alpha_{v,12} = (1000 \sim 2000$ Å) and $\alpha_{v,24} (2000 \sim 4000$ Å) derived from a power-law fitting. Generally, the UV spectra slope becomes harder (higher $\alpha_v$) toward higher bolometric luminosity. On the other hand, when quasars are further grouped into luminosity bins, we find that both $\alpha_{v,12}$ and $\alpha_{v,24}$ show significant anti-correlations with redshift (i.e., the quasar continuum becomes redder toward higher redshift). We suggest that the cosmic dust extinction is very likely the cause of this observed $\alpha_v \sim z$ relation. We build a simple cosmic dust extinction model to quantify the observed reddening tendency and find an effective dust density $n\sigma_v \sim 10^{-5}h$ Mpc$^{-1}$ at $z < 1.5$. The other possibilities that could produce such a reddening effect have also been discussed.

Key words: dust, extinction – quasars: general

1. INTRODUCTION

Observationally, quasars show very similar UV-optical spectra (Francis et al. 1992), which can be characterized by a featureless continuum and a series of broad emission lines (Peterson 1997). At wavelengths longer than the Ly$\alpha$ line, from $\sim 1300$ to $5000$ Å, the continuum of quasars can be well described by a power law $f_\nu \propto \nu^\alpha_v$, where $\alpha_v$ characterizes the continuum slope with a typical value $\sim -0.5$ (Vanden Berk et al. 2001). In terms of $\alpha_v$, more negative $\alpha_v$ means a steeper (or redder, softer) continuum.

There is a general agreement that the UV continuum of higher luminosity quasars is harder (Carballo et al. 1999; Telfer et al. 2002; Davis et al. 2007; however, see also Kennefick & Bursick 2008). On the other hand, there has been a long running debate on the existence of the redshift dependence (evolution) of the quasar continuum. Some studies suggest the slight hardening of the continuum toward higher redshift (Carballo et al. 1999; Kennefick & Bursick 2008), while others find hardly any evolution (Kuhn et al. 2001; Pentericci et al. 2003) or even reverse (Wright 1981).

Several mechanisms could cause the redshift dependence of the quasar continuum, e.g., the evolution of the accretion process (Kennefick & Bursick 2008) and/or the evolution of the dust component. Among them, one of the interesting mechanisms is the intergalactic (cosmic) dust extinction, which makes the quasar spectra statistically redder at higher redshifts. Indeed, Wright (1981) attributed the redder spectra toward higher redshifts they detected to the effect of the cosmic dust, and concluded that the average line of sight has a cosmic extinction of $A_\nu = 0.85 \pm 0.51$ out to $z = 3$ (however, see also Cheng et al. 1991). Compared to other attempts on probing the cosmic dust extinction (e.g., More et al. 2009; Ménard et al. 2010a), quasars take advantage of their high luminosity and large sample size; therefore, they can be explored to higher redshifts.

In this Letter, we take a large quasar sample from Sloan Digital Sky Survey (SDSS, York et al. 2000) and use the continuum slope of the quasar composite spectrum to probe its redshift dependence, then further explore its implications for the cosmic dust.

This Letter is organized as follows. In Section 2, we describe the data and method of building the composite spectrum. In Section 3, we report the finding of a significant dependence of $\alpha_v$ on the redshift: redder spectra at higher redshifts. In Section 4, we build a simple cosmic dust extinction model to quantify the observed reddening effects. In Section 5, we discuss other possibilities. Finally, we present our conclusions in Section 6. Throughout this Letter, we adopt the cosmological parameters $\Omega_L = 0.7$, $\Omega_M = 0.3$, and $h = 0.7$.

2. DATA

The SDSS legacy survey provides a database of quasar samples that includes photometries in $u, g, r, i$, and $z$ bands and spectra from 3800 to 9200 Å with resolutions of about 2000 (York et al. 2000). In the SDSS DR7 quasar catalog, Schneider et al. (2010) compiled 105,783 quasars that are more luminous than $M_i = -22.0$ and have at least one emission line with FWHM larger than 1000 km s$^{-1}$ or have interesting/complex absorption features. This catalog provides the basic database for our study.

Accompanying the DR7 quasar catalog, there are other value-added catalogs. Hewett & Wild (2010) recalculated the redshift of quasars and reduced the systematic effects of the redshift to the level of 30 km s$^{-1}$ per unit redshift. Wild & Hewett (2010) improved the sky subtraction in the red wavelength band. After measuring the spectroscopic features, Shen et al. (2011) calculated the implied physical parameters (e.g., the bolometric luminosity, black hole mass, and Eddington ratio) for each quasar.

In this study, we take the spectra from Wild & Hewett (2010) and use the improved redshifts from Hewett & Wild...
(2010). We exclude the quasars with broad absorption lines from our analysis according to the flags in Shen et al. (2011). The radio-loud quasars show significantly redder continua than radio-quiet ones (Labita et al. 2008) and the fraction of them changes with both redshift and luminosity (Jiang et al. 2007). For these reasons, we also remove them. Therefore, our final sample with calculated bolometric luminosity includes 91,131 objects.

2.1. Composite Spectrum

We first correct the galactic reddening for each quasar using the SFD map (Schlegel et al. 1998) and the reddening curve of Cardelli et al. (1989). Then, we mask bad pixels and shift the spectra to their rest frame according to the redshifts of Hewett & Wild (2010). Next, we follow Vanden Berk et al. (2001) to make the quasar composite and calculate the statistical error for the composite spectrum by dividing 68% semi-quantile to the square of the contributing number at each wavelength.

The composite spectrum of all 91,131 quasars is shown in Figure 1 as the blue line. For comparison, the composite spectrum by dividing 68% semi-quantile to the square of the contributing number at each wavelength.

In the UV-Opt band, the quasar continuum can be very nicely characterized by a single power law ($E \propto \nu^{-\alpha}$) and is usually fitted from continuum windows. In Vanden Berk et al. (2001), two continuum windows, 1350–1365 Å and 4200–4230 Å, have been adopted, which avoid the Ly$\alpha$ line at shorter wavelengths and contamination from the host galaxy at longer wavelengths. However, this range is too long to be covered by any single SDSS spectrum at any given redshift. Similar to Davis et al. (2007), we add a new continuum window 2210–2230 Å. With this configuration of continuum windows and the 3800–9200 Å wavelength range of SDSS quasars, the far-UV slope $\alpha_{24}$ and the near-UV slope $\alpha_{24}$ can be fitted for quasars in the redshift intervals $1.80 < z < 3.15$ ($n = 22251$) and $0.71 < z < 1.19$ ($n = 18068$), respectively.

3. RESULT

3.1. Trend of $\alpha_\nu$ with Bolometric Luminosity

We bin the quasars into four bolometric luminosity ($L_{\text{bol}}$) bins with a bin size of 1 dex from $10^{44}$ erg s$^{-1}$ to $10^{48}$ erg s$^{-1}$ and then make composites respectively. To show the possible variance of the composites more clearly, each composite spectrum is further divided by the global composite spectrum (blue line in Figure 1) and normalized at 3000 Å. The results are shown in Figure 2.

The quasar composite spectra change with $L_{\text{bol}}$ significantly, where the higher $L_{\text{bol}}$ quasars have systematically harder continua. We calculate the continuum slopes ($\alpha_{12}$ and $\alpha_{24}$) for each composite spectrum and plot them as a function of $L_{\text{bol}}$ in the sub-panel of the figure. The $\alpha_{12}$ and $\alpha_{24}$ values are close at high $L_{\text{bol}}$ and show similar trends with luminosity. At the low luminosity side ($\log L_{\text{bol}} < 47$), the change of the continuum slope with luminosity is very significant, while at the high luminosity side ($\log L_{\text{bol}} > 47$), quasar continua roughly keep a constant slope ($\sim 0.5$).

The redder spectra of lower luminosity quasars can hardly be explained by the accretion disk model, where the peak of the big blue bump moves toward lower frequency (longer wavelength) with increasing luminosity (Hubeny et al. 2000; Davis et al. 2007). As discussed in Davis et al. (2007), this discrepancy could be alleviated by assuming a higher intrinsic dust extinction in low luminosity quasars. Indeed, there is observational evidence that the low luminosity AGNs have higher intrinsic dust extinction (e.g., Gaskell et al. 2004). Such a luminosity dependent intrinsic dust extinction scenario is also consistent with a receding dust torus model (Simpson 2005; Gu 2013). However, even if the dust extinction is independent of the quasar luminosity, quasars with higher extinction will also show lower luminosity and redder UV spectra. Such a selection effect may also partly explain the $\alpha_\nu - L_{\text{bol}}$ relation we observed.
of quasars available for composite. The minimum number of quasars to make a composite spectrum is set to 20. The results are shown in Figure 4, where the spectral slopes are plotted against redshift with diamonds (αν_{1/2}) and triangles (αν_{24}). The continuum slopes within the same L_{bol} bin are connected with lines, while different L_{bol} bins are represented by different colors. We find that in any given L_{bol} bin, quasars at higher redshifts have systematically redder UV continuum slopes (for both αν_{1/2} and αν_{24}).

This result clearly identifies the existence of the redshift dependence of quasar spectral slopes and implies that the previous debates are probably driven by redshift selection bias.

4. MODELING THE REDSHIFT DEPENDENCE OF THE QUASAR CONTINUUM SLOPE WITH COSMIC DUST EXTINCTION

As we mentioned in the Introduction, the cosmic dust extinction is a very interesting mechanism that can make the quasar continua systematically redder at high redshift. Therefore, it is quite natural to introduce a cosmic dust extinction model to explain the results we obtained in Figure 4. Other possibilities will be discussed in Section 5.

We start from a toy model, which assumes that dust is uniformly distributed along the line of sight. Considering the intervening dust has a comoving number density of n, the optical depth of the cosmic dust to the photons with wavelength λ₀ emitted from a quasar at redshift z_Q is

\[ \tau(\lambda_0) = \int_0^{z_Q} n_\sigma \left( \frac{1 + z_\sigma}{1 + z} \right) D_H \frac{(1 + z)^2}{E(z)} dz, \]

where \( D_H = cH_0 \), \( E(z) = H(z)/H_0 \), and \( \sigma(\lambda) \) is the cross section of dust absorbers at wavelength \( \lambda \) (More et al. 2009). We assume that the properties of the absorbers do not evolve with redshift and \( \sigma(\lambda) \) is scaled by the cross section of the absorber at 5500 Å, \( \sigma_v \):

\[ \sigma(\lambda) = \sigma_v \cdot \epsilon(\lambda)/\epsilon(5500 \text{ Å}), \]

where \( \epsilon(\lambda) \) stands for the extinction law.

We also assume that the intrinsic continuum of quasars in the UV-Opt band can be characterized by a pure power-law form \( f_\nu = \nu^\gamma \). Quasars are put to their redshifts z_Q, and then, their observational spectral continuum can be rebuilt and slopes \( \gamma \) can be measured after considering the cosmic dust extinction from \( z = z_Q \) to \( z = 0 \). To mimic the observation, we also fit the continuum slopes in different wavelength ranges for quasars at different redshifts (\( \alpha_{νz} \) for \( z_Q > 1.5 \) and \( \alpha_{νz} \) for \( z_Q < 1.5 \)). In this toy model, besides the extinction law, we have two free parameters, one is the combined parameter \( n\sigma_v \), which represents the effective density of the cosmic dust particles, and the other is \( \alpha_v \), the intrinsic quasar continuum slope.

We have little prior knowledge of the template extinction law of the cosmic dust. As the 2175 Å extinction bump is rarely seen in other galaxies, an SMC-type extinction curve is preferred. In this study, we test the featureless SMC extinction law first. We choose sets of representative values of \( \alpha_v \) and show the predicted \( \alpha_{νz} \) as a function of \( z_Q \), which are represented by the dashed parallel lines in Figure 4. Here, \( n\sigma_v = 2 \times 10^{-24} \text{ h Mpc}^{-3} \) is tuned to match the observed \( \alpha_{νz} = -\gamma \) relation.

As can be seen, our simple cosmic dust extinction model can reproduce the observed \( \alpha_{νz} = -\gamma \) relation at the low redshift range (\( z < 1.5 \)) very well. At high redshift, our model
5. DISCUSSION: OTHER POSSIBILITIES

In this section, we discuss whether there are any other explanations to the redshift dependence of the quasar continuum slopes other than the cosmic dust.

5.1. Evolution of Intrinsic Properties?

In Section 3.1, we have argued that the internal dust extinction might be the cause of the \( \alpha_{\nu} - \log L \) luminosity trend that we observed. Could it also be responsible for the \( \alpha_{\nu} - z \) relation? In general, we know that metal and dust are accumulated through various processes in the galaxy evolution, e.g., dust formation in Type II supernova and asymptotic giant branch stars (Asano et al. 2014). Therefore, galaxies at lower redshifts will typically have more dust. This global trend is opposite to the \( \alpha_{\nu} - z \) relation we observed for quasars.

However, we know that quasar host galaxies are atypical. Many observations have shown the presence of large dust mass in high redshift \( z > 4 \) quasars; though, the origin of the large amount of dust in such early epochs is unclear (Valiante et al. 2011, and references therein). Moreover, there are also clues that the extinction curves of high redshift \( z > 4 \) quasars might be different from their lower redshift counterparts (e.g., Nozawa et al. 2015). Despite the variations, we have not yet found any statistical evidence that quasars at higher redshifts show systematically higher intrinsic extinctions, at least for the redshift range we probed \( 0.7 < z < 3.2 \). Nevertheless, we emphasize that such a possibility still opens.

Besides the possible evolution of the intrinsic dust, could other physical properties (e.g., the black hole accretion process) of quasars evolve? Since the black hole accretion is a local physical process, we do not expect that they show significant redshift evolution effects once their basic physical parameters are fixed (e.g., black hole mass or accretion rate). In this work, we group quasars into \( L_{\text{bol}} - z \) bins and do not further consider the variation of other physical parameters. However, we have tested whether, even after constraining quasars to small black hole mass \( M_{\text{BH}} \) and Eddington ratio \( L_{\text{Edd}} / L_{\text{bol}} \) ranges \((0.1 \text{ dex})\) in the original 2D \( L_{\text{bol}} - z \) bins, the anti-correlation between \( \alpha_{\nu} \) and redshift still exists.

5.2. Host Galaxy Contamination?

Quasars are hosted by galaxies, but they outshine them in most cases. However, for the low luminosity quasars at low redshift, the contamination of starlight might still be significant, especially at the near-UV band, i.e., \( \alpha_{\nu,24} \). For a log\( L_{\text{bol}} \) \( \sim 45.75 \) quasar, a bright star-forming host galaxy with \( M_{\star} = -23 \) contributes \( \sim 20\% \) of the flux in the \( 2000 \sim 4000 \text{ Å} \) range. More than that, the redshift range of the near-UV band we probed is from \( z = 0.7 \) to \( z = 1.1 \). This is the time when the cosmic star formation rate (SFR) starts to decrease. Therefore, it is possible that there are larger contributions of starlight at higher redshift, so that makes the quasar spectra look redder.

To test this possibility, we generate a series of model galaxy spectra at different redshifts according to the cosmic star formation history given in Madau & Dickinson (2014) and their luminosities are assumed to be \( M_{\star} = -23 \). We then combine the galaxy spectra at different redshifts with the composite spectrum of log\( L_{\text{bol}} \) \( \sim 45.25 \) quasars. Again, we measure the \( \alpha_{\nu,24} \) for the synthetic quasar+galaxy spectra at different redshifts. We find that, globally, \( \alpha_{\nu,24} \) becomes smaller (redder) when the galaxy spectra is combined into the quasar spectrum.

(SMC extinction curve and \( n_{\sigma_{V}} = 2 \times 10^{-5} \text{ Mpc}^{-1} \)) predicts a much steeper \( \alpha_{\nu,12} - z \) relation than that observed. This discrepancy can be easily solved by adopting either a lower \( n_{\sigma_{V}} \) at \( z > 1.5 \) or a shallower extinction curve at a far-UV wavelength. To keep our model simple, we test the later possibility. Indeed, there are studies suggesting that the extinction curves in quasars are flatter in the UV (Czerny et al. 2004; Gaskell et al. 2004). We take the flat reddening curve from Gaskell & Benker (2007; hereafter, GB07), which is quite similar to the Milky Way extinction law, except for the lack of a 2175 Å bump. We show the GB07 dust extinction models with the same \( n_{\sigma_{V}} = 2 \times 10^{-5} \text{ Mpc}^{-1} \) as the dotted lines in Figure 4. As expected, the GB07 extinction curve matches the observation much better than the SMC extinction curve at \( z > 1.5 \).

In order to have a more intuitive impression of the cosmic dust extinction, we take the GB07 dust extinction model and calculate the observer-frame extinction \( A_{V} \) and reddening \( E(B-V) \) as a function of source redshift. The \( A_{V} \) and \( E(B-V) \) are plotted in the upper and lower panels of Figure 5 respectively. In this plot, we also show the cosmic extinction constrained from a few other measurements for comparison. The dashed line shows the constant comoving dust extinction model of Ménard et al. (2010a), which is constrained from the statistical detection of dust reddening around galaxies up to large scales. The other observational constraints are also extracted from Figure 9 of Ménard et al. (2010a), which includes the results from measuring the excess scatter seen in higher redshift quasar colors (Mörtsell & Goobar 2003), using the Tolman test (More et al. 2009), combining constraints from luminosity distances and \( H(z) \) (Avogastidis et al. 2009), and using Mg ii absorbers (Ménard et al. 2008; see Appendix C of Ménard et al. 2010a for details). Further study about the impact of cosmic dust on supernova cosmology can be found in Corasaniti (2006) and Ménard et al. (2010b).
continuum. However, on the other hand, we do not find that the combined spectra get redder toward high redshift. The reason is that, while going to the higher redshifts from $z \sim 0.7$ to 1.1 because of the higher SFR, not only does the contribution of the starlight in the near-UV band become larger, but the near-UV band spectrum of the galaxy itself also becomes bluer.

5.3. Quasar Color Selection Bias?

SDSS quasars are selected using a complicated color-based algorithm (Richards et al. 2002). Quasar candidates at high and low redshift are selected based on different color–color diagrams. Therefore, the color-selection criteria might introduce biases to the intrinsic colors of quasars at different redshifts. For example, is it possible that the redder quasar continua at higher redshifts are caused by the missing of red quasars at low redshift or vice versa?

To test this possibility, we take the reddest (the last magenta diamond in Figure 4) composite spectrum and put it at different redshifts (from $z = 3$ to 0) and calculate their observed colors. We do the same thing for the bluest one (the first green triangle). We find that the tracks of the colors of these two composites along the redshift still assemble in the quasar color–color selection area. From this test, we argue that there is no significant selection bias in the colors of quasars at different redshifts in SDSS.

6. CONCLUSION

In this Letter, we use a large non-BAL radio-quiet quasar sample from SDSS DR7 to study the redshift and bolometric luminosity dependence of quasar continuum slope by means of the composite spectrum. Consistent with previous studies, we find that the UV-Opt spectrum becomes harder toward higher bolometric luminosity, and we suggest that the internal dust reddening might be the main reason for this luminosity dependence.

When the bolometric luminosity is controlled, we find that the quasar UV continuum slope is anti-correlated with redshift (redder at higher redshift). We propose that the redshift dependence of the quasar UV slope might be caused by the reddening of the cosmic dust. We build a simple cosmic dust extinction model to quantify the reddening of the quasars. Based on our model, we find that an effective dust density $n\sigma_v \sim 10^{-5} \text{h Mpc}^{-1}$ at $z < 1.5$ can reasonably reproduce the $\alpha_{\text{UV}} - z$ relation. The $\alpha_{\text{UV}} - z$ relation at high redshift ($z > 1.5$) can also be easily reproduced by using a shallow extinction curve or adopting a smaller effective density of the cosmic dust. The cosmic dust extinction constrained from our model is globally consistent with the constraints from other independent measurements, and has reached an unprecedented high redshift ($z \sim 3.2$).

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