**HUBBLE SPACE TELESCOPE REVEALS MULTIPLE SUB-GIANT BRANCH IN EIGHT GLOBULAR CLUSTERS**

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**ABSTRACT**

In the last few years many globular clusters (GCs) have revealed complex color–magnitude diagrams, with the presence of multiple main sequences (MSs), broad or multiple sub-giant branches (SGBs) and MS turnoffs, and broad or split red giant branches (RGBs). After a careful correction for differential reddening, high-accuracy photometry with the Hubble Space Telescope (HST) presented in this paper reveals a broadened or even split SGB in five additional Milky Way GCs: NGC 362, NGC 5286, NGC 6656, NGC 6715, and NGC 7089. In addition, we confirm (with new and archival HST data) the presence of a split SGB in 47 Tuc, NGC 1851, and NGC 6388. The fraction of faint SGB stars with respect to the entire SGB population varies from one cluster to another and ranges from ~0.03 for NGC 362 to ~0.50 for NGC 6715. The average magnitude difference between the bright SGB and the faint SGB is almost the same at different wavelengths. This peculiarity is consistent with the presence of two groups of stars with either an age difference of about 1–2 Gyr or a significant difference in their overall C+N+O content.

**Key words:** globular clusters: individual (NGC 104, NGC 1851, NGC 362, NGC 5286, NGC 6388, NGC 6656, NGC 6715, NGC 708) – stars: Population II

**Online-only material:** color figures

1. INTRODUCTION

Recent photometric studies have revealed unexpectedly complex color–magnitude diagrams (CMDs) in many globular clusters (GCs), indicating that these stellar systems are not as simple as we have been assuming for decades (see Piotto 2009 for a recent review).

ω Centauri is the most famous example of a GC hosting complex multiple stellar populations. It has been known since the late 1990s that its CMD shows multiple red giant branches (RGBs; Lee et al. 1999; Pancino et al. 2000), sub-giant branches (SGBs e.g., Bellini et al. 2010), and multiple main sequences (MSs; Anderson 1997; Bedin et al. 2004).

To date, multiple or broad RGBs have been observed in nearly all the GCs that have been observed with good signal to noise in the appropriate photometric bands (e.g., Marino et al. 2011; Yong et al. 2008; Lee et al. 2009; Lind et al. 2011). Recent studies also suggest that multimodal MSs could be quite common among GCs. In addition to the spectacular case of NGC 2808, which shows three distinct MSs (Piotto et al. 2007), double and triple MSs have been observed in several GCs, including NGC 104, NGC 6752, and NGC 6397 (Anderson et al. 2009; Milone et al. 2010, 2012a, 2012b) and have been associated with stellar generations with a different content of helium and light elements (e.g., Norris 2004; Piotto et al. 2005; D’Antona et al. 2005).

Also the CMDs of many stellar clusters in the Large and the Small Magellanic Cloud (LMC, SMC) are not consistent with single stellar populations (Bertelli et al. 2003; Mackey et al. 2008). Milone et al. (2009a) analyzed 16 intermediate-age clusters in the LMC and found that at least 11 of them (i.e., about 70% of the whole sample) exhibit a wide spread or a split around the main-sequence turnoff, which is consistent with the presence of multiple or prolonged star formation episodes.

Spectroscopic studies have long shown that most of the GCs exhibit some correlations and anticorrelations among light-element abundances (such as the Na–O anticorrelation; Kraft 1979, 1994; Ramírez & Cohen 2002). The fact that light-element variations have also been observed among unevolved stars (e.g., Cannon et al. 1998; Gratton et al. 2001) indicates that they have a primordial origin (see Gratton et al. 2004 for a review).

However, it must be noted that spectroscopic analysis is necessarily limited to a small sample of (bright) stars, and therefore allows us to identify stellar generations which may constitute only a small fraction of the cluster populations. Often spectroscopy investigations cannot follow multiple stellar generations in all evolving sequences (in particular along the MS and the white dwarf cooling sequence). Information on multiple stellar generations is maximized when spectroscopic and photometric data can be used together. Otherwise, we must rely on photometry for a complete analysis of multiple populations (relative fraction, radial distribution, main chemical properties), which manifest themselves in different ways, in different clusters and different evolutionary parts of the CMD.

The multiple populations in NGC 1851 and NGC 104 manifest themselves most prominently in terms of a splitting
of the SGB (Milone et al. 2008, 2012b; Anderson et al. 2009). NGC 6388 also shows hints of such a splitting as well (Piotto 2008; Moretti et al. 2009). These SGB splits have been interpreted as indicating two groups of stars with either an age difference of about 1–2 Gyr or a significant difference in their overall C+N+O content (Cassisi et al. 2008; Ventura et al. 2009; Di Criscienzo et al. 2010).

In this paper we present detection of the broad (and most likely split) SGBs in five additional Milky Way GCs, NGC 5286, NGC 6656, NGC 6715, and NGC 7089, and confirm the presence of a double SGB in NGC 6388, NGC 104, and NGC 1851. In a companion paper based on the spectroscopy of stars selected from the CMDs published in this work, we have found that the two SGBs of NGC 6656 (M22) are made of stars with a different content of iron, s-process elements, and C+N+O (Marino et al. 2009, 2012). A bimodality in s-elements has also been observed along the RGB of NGC 1851 and associated with the double SGB of this cluster (e.g., Yong & Grundahl 2008; Villanova et al. 2010; Lardo et al. 2012).

This paper is organized as follows. In Section 2 we describe the data set, the photometric reduction, the zero-point calibrations, the selection of stars with high-quality photometry, and the differential-reddening correction. The initial detection of the SGB broadenings is presented in Section 3. We then proceed to study the SGBs in increasing detail. We first use new and archival material (1) to derive proper motions to exclude field objects (Section 4) and (2) to provide confirmation of the SGB broadenings from several independent data sets (Section 5). Section 6 then examines these SGBs through a variety of bandpasses. Finally, in Section 7, for each cluster we compare the fractions of stars in the different SGBs with the distribution of stars along the horizontal branch (HB) in the hope of identifying the same populations in the different evolutionary branches (Section 8). Section 9 contains the summary of results and an examination of open questions.

2. OBSERVATIONS AND DATA REDUCTION

We have used images taken with the Wide Field Planetary Camera 2 (WFPC2), the Wide Field Channel of the Advanced Camera for Surveys (WFC/ACS), and the ultraviolet and infrared channels of the Wide Field Camera 3 (UVIS and IR/WFC3) on board the Hubble Space Telescope (HST). These data sets include both proprietary images (GO11233, GO11739, GO12311, PI: Piotto) and data that we retrieved from the STScI archive. In Table 1 we give a summary of the adopted data sets indicating the cluster ID, the epoch of the observation, the number, and the duration of the single exposures, the filters, the program ID, and the program PI.

The astrometry and photometry of WFPC2 images have been carried out for each chip, filter, and epoch independently, by adopting the method described by Anderson & King (2000) based on the effective-point-spread-function (PSF) fitting. We corrected for the 34th row error in HST’s WFPC2 cameras (see Anderson & King 1999 for details) and used the distortion solution as given by Anderson & King (2003). Photometric calibration has been done according to the Holtzman et al. (1995) Vega-mag flight system for the WFPC2 camera.

The astro-photometric reduction of ACS/WFC data was done with the software tools described in detail by Anderson et al. (2008). It consists in a package that analyzes all the exposures of each cluster simultaneously in order to generate a single list of stars for each field. Stars are measured in each exposure with a library PSF that is “perturbed” to better match the PSF in that exposure. This routine was designed to work well in both crowded and uncrowded fields and is able to detect almost every star that can be detected by eye. It takes advantage of the many independent dithered pointings of each image and the knowledge of the PSF to avoid including artifacts in the list. Calibration of ACS photometry into the Vega-mag system has been performed following recipes in Bedin et al. (2005) and using the zero points given in Sirianni et al. (2005). For ACS/WFC data coming from the GC Treasury program GO10775 (PI: Sarajedini) we simply used the calibrated catalogs produced by Anderson et al. (2008, see also Sarajedini et al. 2007) using the same procedures.

We measured star positions and fluxes on the WFC3 images with a software mostly based on img2xy_mWFI (Anderson et al. 2006). Details of this program will be given in a stand-alone paper. Star positions and fluxes have been corrected for geometric distortion and pixel area using the solutions provided by Bellini et al. (2011) for WFC3/UVIS and J. Anderson et al. (in preparation) for WFC3/IR.

2.1. Selection of the Star Sample

Individual stars on the images may be poorly measured for several reasons: crowding by nearby neighbors, contamination from cosmic rays, or image artifacts, such as bad pixels, or diffraction spikes. The goal of the present work is to clearly identify multiple populations, which often manifest themselves as a splitting of 0.02 mag or less in the cluster sequences. For this purpose we need to select the best-measured stars in the field (i.e., those with the lowest random and systematic errors), but we also need to have a large enough statistical sample to be able to identify secondary sequences that may have a much smaller fraction of stars than the primary ones.

The software described in Anderson et al. (2008) provides very valuable tools to reach this goal. In addition to the stellar fluxes and positions, it generates a number of parameters that can be used as diagnostics of the reliability of photometric measurements. These include a parameter, q, related to the quality of the fit of the PSF model to the star’s pixels, the difference in position for each star as measured in different filters, rmxxy, the rms of magnitudes measured in different exposures, rmmag, and a parameter, o, which quantifies how much a star is contaminated from neighboring stars’ flux (see Anderson et al. 2008 for the details).

To select the sample of stars with the best photometry, we adopted the following procedure, which is described in more detail in Section 2.1 of Milone et al. (2009a). Since the q and the rms parameters exhibit a trend with the magnitude, we divided the stars into bins of 0.04 mag and calculated for each bin the median of the rms and q parameters and the 68.27th percentile (hereafter σ) by means of the iterative procedure explained in Milone et al. (2009a). We then added to the median of each bin four times σ and interpolated these points with a spline. All the stars that lie below the spline were flagged as well measured. The o parameter does not show a clear trend with magnitude, so we considered all the stars with o < 0.5 as well measured. In the cases of the most crowded clusters (namely NGC 5286, NGC 6388, NGC 6715, and NGC 7089) we have limited our investigation to stars with radial distance from the cluster center larger than 40 arcsec.

The fraction f of stars that pass all the other criteria of selection, with respect to the total number of stars, changes from one cluster to the other, and strongly depends on the data set, and less critically on the luminosity of the star. As an example,
in the case of NGC 6388, which is one of the most crowded GCs of this paper, we have \( f = 0.66 \) for the F606W ACS/WFC GO10775 images and for stars brighter than \( m_{F606W} = 23.0 \). Specifically, \( \sim 78\% \) and \( \sim 77\% \) of the stars pass the selection criteria based on the positions and magnitude rms, respectively, \( \sim 76\% \) of stars pass the criteria based on the \( q \) parameter, \( \sim 78\% \) that based on \( o \), and \( 66\% \) all the criteria above. In the case of NGC 6656, the most sparse GC in our sample, for F606W ACS/WFC images from GO10775 we have \( f = 0.89 \) for stars with \( m_{F606W} < 23.0 \).

2.2. Correction for Differential Reddening, and Zero-point Spatial Variations

The foreground reddening of the GCs studied in this paper goes from 0.05 (NGC 362) to 0.37 (NGC 6388; Harris 1996, 2010). Therefore, variations of reddening are expected within the field of view of our target clusters. Indeed, the CMDs in all clusters reveal that all the CMD sequences are significantly broader than what would be expected from our photometric precision, even taking into account the small unmodelable spatial changes of the PSF which cause photometric zero-point variations usually smaller than 0.01 mag (see Anderson et al. 2008 for details).

Correcting for both differential reddening and the residual spatial variations of the photometric zero point represents a necessary step toward an accurate analysis of the cluster sequences. To obtain these corrections, we applied the method described in Milone et al. (2012c, Section 3). Briefly, we defined the fiducial MS for the cluster and estimated, for each star, how the observed stars in its vicinity may systematically lie to the
red or the blue of the fiducial sequence; this systematic color and magnitude offset, measured along the reddening line, is indicative of the local differential reddening.

As an example, in the upper left panel of Figure 1 we plot the map of differential reddening in the field of view of NGC 6656. The CMD corrected for differential reddening is shown in the upper right panel, while the original CMDs of stars in five, distinct 1000 $\times$ 1000 pixel regions are plotted in the lower panels. The fact that the double SGB is visible everywhere in the field of view further demonstrates that it cannot be an artifact introduced by differential reddening.

In Figure 2 we show some CMDs before and after our differential-reddening correction for six out of the eight clusters considered in this work.

3. MULTIPLE STELLAR POPULATIONS ALONG THE SGB

Figure 3 shows a zoom of the CMD region around the SGB for six of the clusters studied in this paper. Among the several data sets available for each cluster, we used here the ones with the best photometric quality for SGB stars. The most intriguing feature is already evident: the SGB is much broader than expected (indeed, in most cases split) from photometric errors, which are smaller than 0.01 mag for these selected stars. Note that the fraction of stars in the fainter SGBs differs from cluster to cluster, as discussed in detail in Section 7.

3.1. The Multiple SGB of NGC 1851 and 47 Tucanae

Excluding the peculiar case of ω Centauri, we now know from the literature at least two additional GCs that show a SGB that is not consistent with a single stellar population.8

The first is NGC 1851, which exhibits two clearly distinct SGB branches with a faint SGB containing about the 35% of the SGB stars (Milone et al. 2008, 2009b).

The second is 47 Tuc; evidence of multiple stellar populations along the SGB of 47 Tuc came from the analysis of a large number of ACS/HST images by Anderson et al. (2009). These authors found that the SGB exhibits a clear spread in luminosity, with at least two distinct components: a brighter one with a significant spread in magnitude, and a second one about 0.05 mag fainter in the F475W band, containing about 10% of the stars.

Milone et al. (2012b) found that the brighter SGB further splits into two branches, and that the presence of two stellar populations is clearly visible in the MS, RGB, and the HB.

These results have stimulated us to start a deeper investigation using the WFC3/UVIS camera: GO12311 (PI: Piotto). The $m_{F275W}$ versus $m_{F275W} - m_{F814W}$ CMD of NGC 1851, obtained combining these data and archive ones, is shown in Figure 4. This CMD not only confirms the presence of a split SGB, but also it is so far the clearest bimodal SGB in the literature.

In Figure 5 we reproduce Figure 12 from Milone et al. (2012b), which shows the complex SGB of 47 Tuc. In the $m_{F435W}$ versus $m_{F606W} - m_{F814W}$ CMD we see the faint SGB discovered by Anderson et al. (2009) (these stars are colored red). The $m_{F275W}$ versus $m_{F275W} - m_{F336W}$ and the $m_{F275W}$ versus $m_{F336W} - m_{F435W}$ CMDs are plotted in the middle and the right panel and show the other two SGB branches.

Table 2 shows the relevant (for the present paper) parameters for the eight GCs with a significant SGB broadening that we will discuss in the following. Most of them come from Harris (1996, updated as in 2010). HBR is the horizontal branch ratio $HBR = (B - R)/(B + V + R)$, where $B$, $R$, and $V$ are the numbers of blue HB, red HB, and RR Lyrae (from Harris 1996, updated as in 2010). The HBR for NGC 6388 has been calculated from the CMD presented herein.

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8 We note that the SGB of NGC 6441 is also suspected to show two populations, but we postpone details and discussion to a forthcoming paper dedicated to the two anomalous GCs NGC 6388 and NGC 6441 (A. Bellini et al., in preparation) which will be based on HST program GO11739.
Table 2
Main Parameters for the GCs with Split or Spread SGB

| ID       | $R_{GC}$ | $E(B-V)$ | $(m-M)_V$ | HBR   | $M_V$  | [Fe/H]  |
|----------|----------|----------|----------|-------|--------|---------|
| NGC 104  | 7.4      | 0.04     | 13.37    | -0.99 | -9.42  | -0.76   |
| NGC 362  | 9.4      | 0.05     | 14.81    | -0.87 | -8.41  | -1.16   |
| NGC 1851 | 16.7     | 0.02     | 15.47    | -0.36 | -8.33  | -1.22   |
| NGC 5286 | 8.4      | 0.24     | 15.95    | 0.24  | -8.61  | -1.67   |
| NGC 6388 | 3.2      | 0.37     | 16.14    | -0.63 | -9.42  | -0.60   |
| NGC 6656 | 4.9      | 0.34     | 13.60    | 0.91  | -8.50  | -1.76   |
| NGC 6715 | 19.2     | 0.15     | 17.61    | 0.75  | -10.1  | -1.58   |
| NGC 7089 | 10.4     | 0.06     | 15.49    | 0.96  | -9.02  | -1.62   |

4. PROPER MOTIONS

The stellar fields analyzed in this paper are all located within a few arcminutes from the cluster centers. As a consequence, in all the cases, the number of field stars is negligible with respect to the cluster members. However, while in NGC 5286, NGC 6388, NGC 6656, and NGC 6715 both SGBs are well populated, and therefore well distinguishable from field stars, in NGC 362 and NGC 7089 the faint SGB (fSGB) contains only a small fraction of the total number of SGB stars. For these two clusters the effect of the field contamination is more relevant for the assessment of the significance of the fSGB. One of the most obvious advantages of having more than one epoch of observations is the possibility to measure the proper motions of stars. In the following, we use proper motions to show that, in all clusters, both the fSGB and bright SGB (bSGB) belong to the cluster, and cannot be associated with field stars.

For NGC 362, NGC 5286, NGC 6388, NGC 6656, and NGC 7089 we have used the proper-motion measurements from Milone et al. (2012c). For NGC 6715 we determined proper motions from GO6701 (hereafter epoch 1), GO10775 (epoch 2), and GO10922 (epoch 3) data. To do this, we followed the procedure that has been used for the other clusters by McLaughlin et al. (2006), Bedin et al. (2008), and Anderson & van der Marel (2010).

Briefly, we have adopted as reference frames the frames defined by Anderson et al. (2008) for the GO10775 data set,
Figure 3. CMDs of six out of the eight GCs studied in this paper. Only stars which successfully passed all the selection criteria have been plotted. In the insets, we show the Hess diagram for the region around the SGB.

which have $X$ increasing from east to west, and $Y$ from south to north. We corrected for distortion the coordinates of each star measured in each exposure, and transformed the average position for each star in each of the three epochs into the master frame ($x^{i,j}, y^{i,j}$, $i = 1, 2, 3$).

To minimize the effects of any residual distortion, we applied local transformations using a local subsample of stars. To determine the transformation for each star, we selected the closest stars to the target star as local reference stars. The corresponding 55 pairs of coordinates in the two frames are used to determine the least-squares linear transformation from one coordinate system to the other. Naturally, we excluded the target star in its own transformation.

We used linear transformations in the form

\begin{align}
X^{N,i} &= a(x^{N,i} - x_0) + b(y^{N,i} - y_0) + X_0, \\
Y^{N,i} &= c(x^{N,i} - x_0) + d(y^{N,i} - y_0) + Y_0,
\end{align}

where $X^{N,i}, Y^{N,i}, i = 1, 2, 3$ are the coordinates of the target stars in the distortion-corrected master frame, while $x^{N,i}, y^{N,i}$,
by identifying all the stars that, on the basis of their position in the CMD, are probable cluster members and obtained a crude proper-motion estimate by using a local transformation based on this sample. Then we have iteratively excluded from this list all the stars that did not have cluster-like proper motions (proper motion > 2.5σ, where σ is the proper-motion dispersion of cluster members), despite their proximity to the cluster sequences. This ensures that the relative motions of cluster stars should, on average, be zero.

Results (and proper-motion selection criteria) are shown in Figures 6 and 7. In the left panel we show the CMD for all the stars for which proper-motion measurements are available. The second column of the panels shows the proper-motion diagrams of the stars for four different magnitude intervals. The blue and red circles are drawn in order to select two groups of stars that have member-like and fieldstar-like motions, respectively. The red circle size has been chosen by eye with the criterion of rejecting the most evident field stars that are plotted in red in the CMD in the left panel.

It should be noted that in our study it is more important to have a pure cluster sample than a complete one. Therefore, we fixed the radius of blue circles at 2.5σ, where σ is the proper-motion dispersion in each dimension. If we assume that proper motions of cluster stars follow a bivariate Gaussian distribution, each circle should include 95% of the cluster members in each magnitude interval. The panels in the third column show the CMD of our chosen cluster stars, and the rightmost upper panel is a blowup of the CMD region around the SGB. In the rightmost lower panel we mark in black the location of stars with cluster-like motion, and in red field stars. In all cases, the stars in both the fSGB and bSGB regions have cluster-like proper motion and cannot be attributed to a field population.

5. CONFIRMING THE SPLIT/SPREAD SGB WITH INDEPENDENT DATA SETS

In this section we make use of a larger set of HST photometry to further confirm and study the SGB spread identified in Figure 3. Figures 8 through 13 present the multi-filter analysis for six out of the eight clusters considered in this work; we describe the procedure in detail here for NGC 362. Panels (a) of Figure 8 show the three CMDs of NGC 362 that can be constructed from the three independent data sets we have available. The red line overplotted on each CMD is a fiducial line drawn by hand. We have also calculated the magnitude difference (Δm) between each star and the fiducial line and plotted it (in panels (b)) as a function of color for stars in the color interval delimited by the dashed lines of panels (a).
Figure 6. Leftmost column: F606W vs. F606W−F814W CMD (F435W vs. F435W−F625W in the case of NGC 362) for all stars with available proper motions. Second column: proper-motion diagrams of the stars in the left panels, in intervals of 1.4 mag. Third column: the proper-motion-selected CMD of cluster members (all stars within the blue circles). Rightmost column: zoom of the proper-motion-selected CMD around the SGB. In this figure we show the cases of NGC 362, NGC 5286, and NGC 6388.

(A color version of this figure is available in the online journal.)

In the top panel (b), we divided the SGB as seen in F475W versus (F435W−F625W) from GO10005 into two groups based on the F435W magnitude, and colored the bSGB stars blue and the fSGB stars green. Note that the choice of the two groups of stars is arbitrary, and it is not intended to demonstrate that these two groups correspond to two distinct SGBs. The intent here is to demonstrate that the SGB spread is real and significant in all clusters. In all the other panels we used this color coding for the
same stars. The fact that the green stars lie systematically below the main SGB in all the plots demonstrates that they are indeed intrinsically fainter.

The histograms in panels (c) show the $\Delta_m$ distribution in each different CMD. The fact that the median $\Delta_m$ of fSGB and bSGB stars differs by $7\sigma(\Delta_m)^{10}$ in all the independent data sets demonstrates that the observed spread is real. Panels (d)

10 We indicate with $\sigma(\Delta_m)$ the error associated with $\Delta_m$ as the ratio between the color dispersion measured for all the stars in a given SGB component and the square root of their number minus one.
Figure 8. Panel (a): zoom of the CMD of NGC 362 around the SGB. Panel (b): rectified SGB with the groups of bSGB and fSGB stars colored in blue and green, respectively. Panel (c): distribution of the magnitude residuals ($\Delta m$). Panel (d): footprint of the data sets. The stars used in this analysis belong to the shadowed area. Panel (e) shows the spatial distribution for the bSGB and fSGB stars. We used the same color code for the data set name in panel (a) and its footprint in panel (d).

(A color version of this figure is available in the online journal.)

Figure 9. As Figure 8 for NGC 5286.

(A color version of this figure is available in the online journal.)
show the footprints of the various comparison data sets relative to the cluster center. Only stars in the shaded region are used in the analysis presented. Stars within the black circles (where present, for example in NGC 5286) have poor photometric quality because of crowding, and are excluded from our analysis. The spatial distribution of bSGB and fSGB stars is shown in the uppermost right panel (e).

6. A MULTI-WAVELENGTH ANALYSIS OF THE SGB SPLIT/SPREAD

Recent studies have demonstrated that the our ability to detect multiple RGB and MS sequences in GCs can be very sensitive to the particular filter system used to study them. For example, the RGBs of both NGC 6121 and NGC 6752 are clearly bimodal in the $U$ versus $U-B$ CMD, yet there is no evidence for any split or intrinsic color spread of the RGB when they are observed in the $B-I$ color (Marino et al. 2008). Similar multiple RGBs have also been observed in CMDs made with the corresponding Strömgren filters (e.g., Grundahl 1999; Yong et al. 2008). These RGB splits have been interpreted as being related to how CN, CH, and NH bands affect some spectral regions but not others (Marino et al. 2008; Yong et al. 2008). Similarly, the color differences between the multiple MSs of ω Centauri, 47 Tucanae, NGC 6397, and NGC 6752 depend strongly on the particular color baseline used to study them. These MS splits have been attributed to a bimodal distribution in helium abundance.

In this section we take advantage of the huge photometric data set available for each cluster in order to investigate how the SGB morphology changes from filter system to filter system. Although each of our clusters has been observed in a different set of bands, each cluster has enough wavelength coverage to make direct comparisons possible.

The approach we use here is similar to our study of the MS in ω Centauri (Bellini et al. 2010). Our aim will be to trace out
the fiducial sequences for the two SGBs in multiple filter bands and quantify the offset between the sequences as a function of color at a set of points across the SGB. If this difference is relatively constant with wavelength, then it is indicative of a difference in the stellar structure (i.e., radius) for the stars in the two sequences. On the other hand, if the difference varies with wavelength then there could be atmospheric effects going on as well.

Our approach is illustrated in Figure 14 for NGC 1851. For this cluster, we have observations for the same stars through the F275W, F336W, F606W, and F814W filters. In the upper left panel (a), we show the stars in the color system that best separates the populations. For this cluster, that is in F275W versus F275W − F814W.

We associate each star along the SGB with either the bright or the faint population. In the panels on the right (b), we color code the stars by population and plot them in the same color system (F275W−F814W), but with a different photometric band along the vertical axis in each panel. The upper SGB is shown as black points and the lower SGB as medium gray points. We then trace out the upper and lower sequences by specifying a set of fiducial points along each of them.

Finally, we measured the magnitude difference between the fiducial line of the faint and the bright sequences corresponding to the three colors indicated by the blue, green, and red lines. We plot the difference between the faint and bright sequences in each photometric band in the lower left panel (c) for each color. The error bars are indicative of the number and spread of the points that went into the value plotted. It is clear that the separation between the sequences is relatively constant with photometric band and it is also relatively the same for all three groups.
Figure 12. As Figure 8 for NGC 6715.

(A color version of this figure is available in the online journal.)

Figure 13. As Figure 8 for NGC 7089.

(A color version of this figure is available in the online journal.)
In Figures 15–18, we perform the same analysis for NGC 5286, NGC 6388, NGC 6656, and NGC 6715. We have excluded NGC 362 and NGC 7089 from this analysis because the small number of stars in the fSGB does not allow us to obtain a fully reliable fiducial line. All of these show roughly the same behavior: the magnitude difference between the bSGB and the fSGB has almost no dependence on wavelength. This behavior rules out the hypothesis that the observed SGB split could be related to some effects due to molecular bands on the atmosphere (which would affect only specific photometric filters), in contrast to what has been seen on the RGB. Rather it must be due to some difference in the stellar structure (or mass).

We will defer a detailed comparison of our CMDs with theoretical isochrones to a dedicated paper, but it is worth mentioning here that these general results are very similar to what has already been found for NGC 1851 by Cassisi et al. (2008) and Ventura et al. (2009). In particular:

1. If we assume that the two stellar populations represented by the two SGBs have the same—\(\alpha\)-enhanced—chemical composition and that the SGB split (or magnitude dispersion) is due to an age difference alone, stars populating the fSGB should be older by \(\sim 1–2\) Gyr.

2. Alternatively, if the bSGB and the fSGB stars have different chemical compositions, with the fSGB stars being CNO enriched, the stellar groups corresponding to the two SGBs could be—when accounting for the quoted uncertainty on the relative age—nearly coeval, or the fSGB could be slightly younger.

For the clusters analyzed above we found that the SGBs can be characterized as being bimodal or broad in every filter system. This is in contrast to the well-studied case of 47 Tuc, which has been shown to have two close upper SGBs and a more separated lower SGB. In 47 Tuc, we were able to follow the two populations through the entire CMD, from the MS to the SGB, RGB, and HB.

Even though 47 Tuc clearly has a more complicated morphology than these clusters, since the sequences have been studied both photometrically and spectroscopically, it may yet help us understand the simpler phenomenon at work here. In 47 Tuc, the two upper SGBs contain \(~92\%) of the stars at the center. The more populous upper sequence (hereafter mSGB) has been shown to consist of CN-strong/Na-rich/O-poor stars, while the less populous sequence (uSGB) is made up of CN-weak/Na-poor/O-rich stars. The lowest SGB (named lSGB) also appears to be CN-strong/Na-rich/O-poor, like the mSGB (Milone et al. 2012b).

In order to compare the SGB of 47 Tuc with these clusters, in Figure 19 we adapt the procedure introduced in Figure 14 for NGC 1851 to the triple SGB of 47 Tuc. In the CMDs of the left panels, the sample of uSGB, mSGB, and lSGB stars selected by Milone et al. (2012b) are colored green, magenta, and red, respectively. Similar to what was done for NGC 1851, we have calculated for each CMD the magnitude difference between the mSGB and the uSGB, between the lSGB and the uSGB, and between the ISGB and mSGB at the color levels indicated by the three vertical lines. In the left panels we again plotted these magnitude differences as a function of the central wavelength of the different \(m_X\) bands in our data set. We found that the
Figure 15. As Figure 14 but for NGC 5286.

(A color version of this figure is available in the online journal.)

Figure 16. As Figure 14 but for NGC 6388.

(A color version of this figure is available in the online journal.)
Figure 17. As Figure 14 but for NGC 6656.
(A color version of this figure is available in the online journal.)

Figure 18. As Figure 14 but for NGC 6715.
(A color version of this figure is available in the online journal.)
Figure 19. Left panel: zoom in of the CMDs around the SGB of 47 Tuc. Green, magenta, and red points correspond to uSGB, mSGB, and lSGB stars. For clarity we show here only four CMDs. Right panels: magnitude difference between the mSGB and the lSGB (upper panel), the mSGB and the uSGB (middle panel), and the ISGB and the uSGB (lower panel). These magnitude differences are calculated at $m_{F275W} - m_{F814W} = 2.48$ (red triangles), 2.60 (green squares), and 2.80 (blue triangles). These colors are marked by vertical lines on the left.

(A color version of this figure is available in the online journal.)

Figure 20. Scheme of the procedure used to determine the fraction of fSGB and bSGB stars in NGC 6388. Panel (a) is a zoom of the CMD around the SGB; the two lines delimit the SGB portion where the spread is more evident. In panel (b) we have transformed the reference frame of panel (a) and marked with a dashed green line the bSGB fiducial drawn by hand. In panel (c) we plotted stars between the two continuous lines but after subtracting from the X value of each star the X of the fiducial at the corresponding Y. The four panels (d) show the $\Delta X$ distribution for stars in four $\Delta Y$ intervals. The solid lines represent the bi-Gaussian fit. The dispersion of the best-fitting Gaussian is indicated in each box.

(A color version of this figure is available in the online journal.)
Figure 21. As Figure 20 but for NGC 6656.
(A color version of this figure is available in the online journal.)

Figure 22. As Figure 20 but for NGC 6715.
(A color version of this figure is available in the online journal.)
Figure 23. As Figure 20 but for NGC 362.
(A color version of this figure is available in the online journal.)

Figure 24. As Figure 20 but for NGC 5286.
(A color version of this figure is available in the online journal.)
lSGB is about 0.05 mag fainter than the mSGB, as indicated by the filled symbols, and that this magnitude difference is the same, within our error bars, at all wavelengths, similar to what we found for the other clusters studied in this paper. The uSGB is typically ~0.02 mag brighter than the mSGB and 0.08 mag brighter than the lSGB, but their magnitude separation increases to ~0.08 mag and ~0.14 mag in the F336W band (open symbols), respectively. Since the F336W filter includes the NH molecular bands at λ ∼ 3300 Å, we suggest that the latter behavior is due to a higher N content (strong NH band absorption) in mSGB stars.

These results support the findings of Di Criscienzo et al. (2010) and Milone et al. (2012b). According to these authors, the implication is that the uSGB must correspond to the first stellar population with a chemical composition similar to the halo stars, while the mSGB should be made by N/Na/He-rich O/C-poor second-generation stars. Only a small fraction of the second generation is also characterized by an overall C+N+O increase: these stars represent the ISGB.

### Table 3

| ID     | Same Age, Twice C+N+O | Same C+N+O, Δ Age 1–2 Gyr |
|--------|-----------------------|---------------------------|
|        | mSGB ALL              | ISGB ALL                  | mSGB ALL              | ISGB ALL              |
| NGC 362| 0.97 ± 0.01           | 0.03 ± 0.01               | 0.99 ± 0.01           | 0.01 ± 0.01           |
| NGC 5286| 0.87 ± 0.03           | 0.13 ± 0.03               | 0.85 ± 0.03           | 0.15 ± 0.03           |
| NGC 6388| 0.78 ± 0.02           | 0.22 ± 0.02               | 0.90 ± 0.02           | 0.10 ± 0.02           |
| NGC 6656| 0.60 ± 0.04           | 0.40 ± 0.04               | 0.56 ± 0.04           | 0.36 ± 0.04           |
| NGC 6715| 0.47 ± 0.04           | 0.53 ± 0.04               | 0.49 ± 0.04           | 0.51 ± 0.04           |
| NGC 7089| 0.95 ± 0.01           | 0.05 ± 0.01               | 0.97 ± 0.01           | 0.03 ± 0.01           |

### 7. POPULATION RATIO

The fractions of stars in the different generations can provide fundamental constraints on the formation and evolution of these stellar systems. To estimate the numbers of fSGB and bSGB stars, we adopted a procedure similar to the one used by Milone et al. (2009b), and illustrated in Figures 20–25 for six of the clusters studied in this paper.

Briefly, we selected by hand two points on the fSGB ($P_{1, f}$, $P_{2, f}$) and the bSGB ($P_{1, b}$, $P_{2, b}$) with the purpose of delimiting the SGB region where the split is most evident, as shown in panel (a). These two points have been connected with a straight line, as shown in panel (a). Only stars contained within the region between these lines were used in the following analysis. In panel (b) we have transformed the CMD into a reference frame where the origin corresponds to $P_{1, b}$; $P_{1, f}$ has coordinates (1,0), and the coordinates of $P_{2, b}$ and $P_{2, f}$ are (0,1) and (1,1), respectively. As in Milone et al. (2009b), in the following, we indicate as “X” and “Y” the abscissa and the ordinate of this
Figure 26. CMD of six clusters with double or spread SGB. The dashed and solid lines represent the isochrones for the normal population and the extreme CNO-enriched ones, respectively. Best-fitting ages, distance modulus, and reddening are quoted in Table 3.

(A color version of this figure is available in the online journal.)

reference frame. The dashed green line is the fiducial line of the bSGB.

In panel (c) we have calculated the difference between the X value of each star and the X of the fiducial line (ΔX). In the cases of NGC 6388, NGC 6656, and NGC 6715 the histograms in panel (d) are the ΔX distribution for stars in four ΔY intervals (see Figures 20–22). These distributions have been modeled as the sum of two partially overlapping Gaussian functions.
In the cases of NGC 362, NGC 5286, and NGC 7089, where the number of fSGB stars is too small not only to fit with an independent Gaussian but also to distinguish if the fSGB and the bSGB are two distinct populations or the product of continuous star formation episodes. We have arbitrarily drawn the vertical line in panel (c) to separate the groups of fSGB and bSGB stars (see Figures 23–25).

It is important to note that each of the points \( P_{1,b}, P_{1,f}, P_{2,b}, \) and \( P_{2,f} \)—arbitrarily defined with the sole purpose of isolating a group of stars representative of each of the two SGBs—corresponds to a different mass \( (M_{P1b}, M_{P1f}, M_{P2b}, \) and \( M_{P2f}) \). To obtain a reliable measure of the fraction of stars in each of the two populations (hereafter \( f_{\text{SGB}} \) and \( f_{\text{fSGB}} \)) we have to compensate for the fact that the two stellar groups that define the two SGBs cover two different mass intervals \( (M_{P2f} - M_{P1f} \neq M_{P2b} - M_{P1b}) \), due to the different evolutionary lifetimes. Consequently, the correction we have to apply will be somewhat dependent on the choice of the mass function, \( \phi(M) \).

To this end, we can calculate the fraction of stars in each branch as

\[
\begin{align*}
\frac{f_{\text{SGB}}}{f_{\text{fSGB}}} &= \frac{A_0}{A_1} \int_0^{P_{2,b}} \phi(M) dM \quad \text{for the bSGB} \\
\frac{f_{\text{SGB}}}{f_{\text{fSGB}}} &= \frac{A_f}{A_1} \int_0^{P_{2,b}} \phi(M) dM \quad \text{for the fSGB}
\end{align*}
\]

where \( N_{f(b)} = \int_0^{P_{2,b}} \phi(M) dM \) are the observed numbers of stars, \( \phi(M) \) is the adopted mass function, and \( A_0 \) and \( A_f \) are the areas under the Gaussians for the bSGB and fSGB stars. The latter are calculated as the areas of the Gaussians that best fit the bSGB and the fSGB in the cases of NGC 6388, NGC 6656, and NGC 6715, while for NGC 362, NGC 5286, and NGC 7089 we assumed that \( A_0 \) and \( A_f \) correspond to the number of stars on the blue and the red side of the dashed line of panel (c).

As for the dependence on the adopted mass function, we ran the following test. We assumed first a heavy-mass-dominated mass function \( (\alpha = -1.0) \) and then a steep \( (\alpha = 3.0) \) mass function. Even with these extreme assumptions, we found that the mass function effect can change the relative fSGB/bSGB population ratio by a negligible \( 3\% \). Therefore, for simplicity, we adopted a Salpeter (1955) initial mass function for \( \phi(M) \).

Results are listed in Table 3. Columns 2 and 3 list the relative numbers of each population obtained by assuming that the two SGBs have the same age but different C+N+O content (fSGB stars with two times more C+N+O than bSGB ones). The relative numbers of bSGB and fSGB stars listed in Columns 4 and 5 are calculated by assuming for the two SGBs the same overall CNO but different age (\( \Delta \) Age 1–2 Gyr, fSGB older, Figure 26; see Cassisi et al. 2008). We found that by using the different isochrones the resulting fractions of fSGB and bSGB stars change by less than 0.04. In most cases these differences are within our uncertainties.

We found that in five out of six GCs in Table 3 the bSGB contains the majority of the cluster stars, which is also what has been observed in NGC 104 (Anderson et al. 2009) and NGC 1851 (Milone et al. 2009b), bringing the statistics to seven out of eight. The fraction of fSGB and bSGB varies considerably from cluster to cluster: it is a few percent in the cases of NGC 362 and NGC 7089 and \( \sim 50\% \) for the case of NGC 6715.

8. SUMMARY

In this paper we have shown that the Galactic GCs NGC 362, NGC 5286, NGC 6388, NGC 6656, NGC 6715, and NGC 7089 exhibit double or broadened SGBs, similar to those identified in NGC 1851 (Milone et al. 2008) and NGC 104 (Anderson et al. 2009; Milone et al. 2012b). When we compare different CMDs of the same cluster made with different magnitudes and color combinations, we find that the magnitude difference between the bright and the faint SGB components remains approximately constant and does not depend on the filters used. Therefore, we conclude that the split/spread SGB of the GCs studied in this paper can be interpreted in terms of two stellar groups with either a different in age of \( \sim 1–2 \) Gyr or a large difference in the total C+N+O abundance, as previously suggested by Cassisi et al. (2008) and Ventura et al. (2009) for the case of NGC 1851. In the cases of NGC 362, NGC 7089, and NGC 5286, the small number of fSGB stars does not allow us to firmly establish if the two groups of fSGB and bSGB stars correspond to two distinct stellar populations or if the poorly populated fSGBs are just the tail of an extended star formation history.

The fractions of faint and bright SGB stars with respect to the total number of SGB stars change from cluster to cluster, and range from \((0.03:0.97)\) in the case of NGC 362 to \((0.51:0.49)\) for the Sagittarius dwarf galaxy’s GC NGC 6715.

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REFERENCES

Anderson, A. J. 1997, Ph.D. thesis, Univ. California, Berkeley
Anderson, J., Bedin, L. R., Piotto, G., Yadav, R. S., & Bellini, A. 2006, A&A, 454, 1029
Anderson, J., & King, I. R. 1999, PASP, 111, 1095
Anderson, J., & King, I. R. 2000, PASP, 112, 1360
Anderson, J., & King, I. R. 2003, PASP, 115, 113
Anderson, J., Piotto, G., King, I. R., Bedin, L. R., & Guhathakurta, P. 2009, ApJ, 697, L58
Anderson, J., Sarajedini, A., Bedin, L. R., et al. 2008, AJ, 135, 2055
Anderson, J., & van der Marel, R. P. 2010, ApJ, 710, 1032
Bedin, L. R., Cassisi, S., Castelli, F., et al. 2005, MNRAS, 357, 1038
Bedin, L. R., Piotto, G., Anderson, J., et al. 2004, ApJ, 605, L125
Bedin, L. R., Salaris, M., Piotto, G., et al. 2008, ApJ, 679, L29
Bellini, A., Anderson, J., & Bedin, L. R. 2011, PASP, 123, 622
Bellini, A., Bedin, L. R., Piotto, G., et al. 2010, AJ, 140, 631
Bertelli, G., Nasi, E., Girardi, L., et al. 2003, AJ, 125, 770
Cannon, R. D., Croke, B. F. W., Bell, R. A., Hesser, J. E., & Stathakis, R. A. 1998, MNRAS, 298, 601
Cassisi, S., Salaris, M., Pietrinferni, A., et al. 2008, ApJ, 672, L115
D’Antona, F., Bellazzini, M., Caloi, V., et al. 2005, ApJ, 631, 868
di Criscienzo, M., Ventura, P., D’Antona, F., Milone, A. P., & Piotto, G. 2010, MNRAS, 408, 999
Gratton, R. G., Bonifacio, P., Bragaglia, A., et al. 2001, A&A, 369, 87
Gratton, R. G., Sleden, C., & Carretta, E. 2004, ARA&A, 42, 385
Grundahl, F. 1999, in ASP Conf. Ser. 192, Spectrophotometric Dating of Stars and Galaxies, ed. I. Hubeny, S. Heap, & R. Cornett (San Francisco, CA: ASP), 223
Harris, W. E. 1996, AJ, 112, 1487
Harris, W. E. 2010, arXiv:1012.3224
Holtzman, J. A., Burrows, C. J., Casertano, S., et al. 1995, PASP, 107, 1065
Kraft, R. P. 1979, ARA&A, 17, 209
Kraft, R. P. 1994, PASP, 106, 553
Lardo, C., Milone, A. P., Marino, A. F., et al. 2012, A&A, 541, A141
Lee, Y.-W., Joo, J.-M., Sohn, Y.-J., et al. 1999, Nature, 402, 55
Lee, J.-W., Kang, Y.-W., Lee, J., & Lee, Y.-W. 2009, Nature, 462, 480
