Formation of wavy-ring crack in drying droplet of protein solutions

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The formations of desiccation cracks and their patterns in drying droplets of protein solutions are studied experimentally. The solvent evaporation causes the dehydration self-organization phenomenon in colloidal droplets, followed by the formations of desiccation cracks. Two categories of highly ordered crack patterns, which we name “daisy” and “wavy-ring”, are identified in the drying droplets. We explore the shifting of crack patterns from the “daisy” to the “wavy-ring” by varying the concentration of protein droplets. The results show that the concentration correlates with the pattern of deposition film directly, and modulates the periodicity of the crack pattern. We investigate the formations and periodicities of these two kinds of crack patterns, and obtain the scaling law of periodicity of the “wavy-ring” crack pattern. The relationship between the deposition pattern and the highly ordered crack patterns is also examined. This study will help in understanding the formation mechanisms of crack patterns in drying droplets of protein solutions and assist the future design of crack patterns in practical applications.

coffee-ring effect, spiral crack, self-organization, crack pattern, desiccation

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1 Introduction

Desiccation crack is a general phenomenon in nature and has aroused scientists’ attention for centuries. As early as 1917, Kindle [1] studied on mud crack experimentally in the lab and obtained different mud crack patterns by varying the components of mud and the velocity of the desiccation. Drying is one of the most often used methods in thin film preparation [2]. However, along with the drying process, cracks may originate and propagate. Fascinating crack structures and patterns formed by desiccation have been observed in different types of hard film/soft substrate systems [3,4]. In recent years, there has been an increasing number of reports on crack morphologies and final patterns in thin films, such as spiral cracks [5,6], oscillating cracks [7–9], annular cracks [10,11], etc. Kattouf et al. [12] proposed a corresponding model of the nucleation and development to study the generation of perfect periodically hexagonal crack patterns. These attractive desiccation crack patterns have been found useful in traditional art field and industry. Craquelure patterns can help identify the age of oil paintings [13–15]. Preventing the troublesome cracks and developing the crack patterns in practical applications are of more interest, such as the fabrication of nanoelectronic and microfluidic devices [16,17] and industrial applications in printing [18–20].

To utilize desiccation cracks in thin film preparation, understanding the underlying mechanisms of crack pattern formation is of great significance. Experimental and theoretical efforts have been infused into the studies of the formation of these crack patterns. The cracking dynamics and pattern transitions in some colloidal droplets were studied [21–23]. Pauchard et al. [24] obtained both regular and disordered patterns in colloidal suspension depending on the
suspension salinity. Leung et al. [25] and Néda et al. [26] focused on spiral cracks in thin films of drying suspension of precipitate and proposed a mesoscopic spring-block model to simulate this desiccation spiral crack. Wu et al. [27] studied Archimedes spiral cracks in a nanofilm. The conditions that influence the formations of crack patterns were also explored, such as the desiccation direction (by controlling temperature and humidity) [28–31], an electric field [32,33], and a magnetic field [34].

It also has long been known that drying droplets of biological solutions may crack due to the evaporation of the solvent, such as DNA [35], human blood [36,37], human tears [38], protein solutions [39,40], etc. Brutin et al. [36] reported that the patterns formed in droplets of human blood can be used to tell whether persons are in good health. A blood drop of a healthy person will generate regular and ordered crack pattern, in contrast to messy cracks formed in that of a person with hyperlipidaemia or anaemia. Sobac and Brutin [37] also found that the wettability influences the final pattern of a drying blood droplet. Studies on crack patterns of drying droplets of human tears pointed out that these patterns can be used to diagnose eye disease in patients [38]. Golbraikh et al. [40] revealed that crack patterns were phenomenologically the same as an array of cracks and provided a model to describe the formation of this crack pattern from the view of crystallization. However, owing to the complex composition of biological fluids and multi-physical-chemical-mechanical processes, the mechanisms of different crack patterns caused by spontaneous evaporation still stay unexplained. Because of the diversity of cracks, it is difficult to explain the whole details of pattern formation by analytical formulations or a single model.

In this paper, we study the formations of typical patterns in drying droplets experimentally using a protein solution (i.e., aqueous egg-white solutions for representation). Various cracks form quite different patterns in the droplets with different concentrations. We investigate the influence of complete drying process on the final pattern and classify these patterns. Then the formation mechanisms of these crack patterns and their peculiar periodicities are further explored.

2 Materials and methods

To study multifarious cracks and their patterns in drying droplets, we selected a protein solution, i.e., egg-white solution—A typical and common biological fluid, to perform the experiments. The raw egg-white solution is formed primarily by 10% proteins (approximately 148 kinds of proteins and ovalbumin is the most abundant one) dissolved into 90% water. Deionized water was used to dilute the raw egg-white solution. We varied the dilution multiple $\alpha$ with 0, 0.2, 1, 10, 25, 50, 90, 100, 125, 150, 170, 200, 300, 400 and 500 for experimental samples. As a result, the volume concentration of proteins $c$ changed from 10% to 0.19‰, as listed in Table 1.

The experiments were conducted on a vibration-damping platform. Protein droplets of different concentrations with a volume of 2 μL were deposited on the surface of clean silicon wafer Si (100) using a micropipette. Then the droplets evaporated under room temperature (25°C) and ambient pressure (1 atm) with a relative humidity (RH) ~20%. The drying processes were captured using a three-dimensional digital microscope (HIROX KH8700 with MX-mount lens of 5040RZ and 10C) right above the droplets at a frame rate of 24 fps. At the same time, a contact angle meter (Data-physics OCA-20) was used to observe lateral profiles of the droplets in real-time at a frame rate of 0.5 fps. At last, a contact surface profiler (Bruker DektakXT with contact radius $r_c=2.5 \mu$m and contact force $f_c=1$ mN) was employed to measure three-dimensional profiles of the deposition films. The experiments were repeated more than dozens of times.

3 Results and discussion

3.1 Droplet evaporation process

When the droplet was dripped on the surface, the evaporation of solvent started. To explore the evaporation process, we measured the dynamic evolution of contact angles of droplet during the evaporation process. The time required for the whole evaporation was about 5–10 min, which depended on the concentration and the volume of the droplet. Figure 1 presents the evolution of contact angles of the drying droplets with the concentrations 83.33‰ and 0.50‰. As the protein droplets dried, particles (proteins) assembled at the

| Dilution multiple ($\alpha$) | Concentration of proteins ($c$) |
|---------------------------|-------------------------------|
| 0.2                       | 83.33‰                       |
| 1                         | 50.00‰                       |
| 10                        | 9.09‰                        |
| 25                        | 3.85‰                        |
| 50                        | 1.96‰                        |
| 90                        | 1.09‰                        |
| 100                       | 0.99‰                        |
| 125                       | 0.79‰                        |
| 150                       | 0.66‰                        |
| 170                       | 0.58‰                        |
| 200                       | 0.50‰                        |
| 300                       | 0.33‰                        |
| 400                       | 0.25‰                        |
| 500                       | 0.19‰                        |
three-phase contact line [41,42]. Since the particles pinned the contact line onto the substrate, droplets dried under constant area condition. Therefore, the contact angles decreased with the evaporation process proceeding.

At first, the contact angles of these two kinds of droplets (concentrations 83.33‰ and 0.50‰) changed smoothly with little difference. As the evaporation was continuing, the main difference emerged. For the protein droplets with concentration 0.50‰, the contact angles changed continuously, however, those of the protein droplets with concentration 83.33‰ experienced a shift point. The particles accumulated at the interphase boundary and finally aggregated to form a gelled foot when the particles got more concentrated, while the central part of the droplets remained liquid [24]. Supporting material Movie 1 exhibits the dynamic drying processes of droplets with different concentrations.

During the drying process, the relative motion of particles to the solvent causes Stokes drag force acting on particle surfaces. Assuming the protein molecules as equal spheres, we can calculate the Stokes force

\[ F_{\text{drag}} = 3\pi \mu D u, \]

where \( \mu \) is the dynamic viscosity, \( D \) is the average hydrodynamic diameter of a protein and \( u \) is the flow velocity. Taking no account of the interactions of particles, the effective viscosity of the dilute solution increases with the volume concentration of the solute as \( \mu_{\text{eff}} \approx \mu (1 + 5 c/2) \) [43]. Hence, a relatively high concentration will generate a high effective viscosity. As the particles get more and more concentrated, they eventually touch each other. Thus the maximum capillary force between two adjacent particles is expressed as [44]

\[ F_{\text{c,max}} = \frac{2\pi D \gamma \cos \theta}{3}, \]

where \( \gamma \) is the solvent-air interfacial tension and \( \theta \) is the contact angle between the solvent and particle. The evaporation of solvent drives the self-organization of particles in the drying protein droplets and finally forms a thin film on the substrate. Understanding the drying and deposition processes is the first step to investigate the formations of desiccation cracks.

### 3.2 Deposition films and their patterns

At the end of droplet evaporation, the droplets solidified and finally formed annular or circular thin films. As shown in Figure 2, there were four typical deposition patterns observed in our experiments by varying the concentration (negatively correlated with the dilution multiples) of the protein solutions. The lower the concentration became, the more obvious the coffee-ring effect was. This is ascribed to the competition among different flows in the droplets. Figure 3(a) displays three flows [45], namely the radial flow, the Marangoni recirculating flow and the vertical flow. The first flow, whose magnitude depends on the ratio of evaporative mass flux and the density of droplets [46], tends to form an annular deposition pattern. The second flow resulting from the surface tension gradient [47] leads to a mountain shape. While the last flow gives rise to a flat film. Driven by Derjaguin-Landau-Verwey-Overbeek (DLVO) interactions, the particles move toward the substrate [48]. The velocity of this flow is estimated as

\[ V_D \approx 2 F_D / 6 \pi \mu D, \]

where \( F_D \) is the DLVO force that is a long-range interaction and refers to the algebra sum of van der Waals and the electrostatic forces [49]. Shape of the droplet changes during the evaporation as illustrated in the schematic of droplet profiles in Figure 3(b). In our experiments, all deposition films had coffee ring, however, the thickness of the film and the width of the coffee ring were quite different. According to Figure 3(c), to quantitatively examine the relationship between the deposition pattern and the concentration, we chose two dimensionless parameters to depict the deposition pattern, i.e.,

\[ \chi_L = L / R_0, \]

that refers to the coffee-ring width normalized by the initial droplet radius and

\[ \chi_H = H_c / H_{\text{max}}. \]

Figure 3(d) reveals that both \( \chi_L \) and \( \chi_H \) increase with the solution concentration.

### 3.3 Desiccation cracks and their patterns

As the deposition process finished and the drying was going on, desiccation cracks originated in the drying film. A fully desiccated droplet consisted clearly of two parts, i.e., the coffee ring and the central part. In these two parts, we discovered quite distinct desiccation cracks and a few highly ordered crack patterns (see Figure 4). These typical...
The morphologies of crack patterns are divided into two broad categories, according to whether their cracks propagated into the central part of the film or not, which we name “daisy” (Figure 4(a) and (b)) and “wavy-ring” (Figure 4(c) and (d)). The Figure 4(e) is a high-definition picture of a “wavy-ring” crack pattern. In this section, we display the details and formations of these two patterns.

3.3.1 The “daisy” pattern

The “daisy” pattern is mainly formed by uniformly arranged radial cracks that originate at the periphery and propagate towards the center. This category of pattern appeared when the concentration of droplets exceeded ~9‰ that was relatively high. It was also observed in other drying colloidal solutions with high concentrations [24]. Besides the radial cracks, curved cracks, spiral cracks, and chaotic cracks were also observed in one drying protein droplet in our experiments, as detailed in Figure 5(a). Curved cracks originated at the perimeter of the drying droplet (Figure 5(b)), and then propagated into the center of the dried protein film radially (Figure 5(c)). When these radial cracks were inclined to stop, they would deflect at the center where cracks were chaotic (Figure 5(d)). In addition, during the drying process, tensile stress generates in the film [50]. Here the residual stress has gradient distribution through the thickness of the film. As a result, cracks generate at the bottom, and then propagate to the surface of the film. More details of the chaotic cracks in our experiments are visible in Figure 5(e), where obscure cracks under the film surface are also demonstrated. Movie 2 presents the formation of the “daisy” pattern.
As discussed previously, for a drying droplet with relatively high concentration, a gelled film develops at the triple contact line; by contrast, the central part is still in liquid state during the drying process. Consequently, a humidity gradient generates along the radial direction. These two parts are set apart by a compact front that moves towards the center point continuously. Following the moving front, radial cracks initiate at the edge of the droplet and grow, as shown in Figure 5(f).

We assume that the drying film is under the in-plane stress $\sigma''$, which is caused by the evaporation and proportional to the capillary pressure. To calculate the strain energy release rate $G$, we need to look at how a single crack releases the stress. Here we define a coordinate system $Oxyz$ located at the crack tip. The thickness direction is defined as the $z$ axis. A crack propagates along the direction of the positive $x$ axis. The stresses released by the crack decay along the normal direction to the crack surface, i.e., the $y$ axis [51]

$$\frac{d\Delta\sigma''}{dy} = -\frac{\Delta\sigma''}{l},$$

where $\Delta\sigma''$ is normal to the crack, $y$ is the normal distance to the crack surface, and $l$ denotes the characteristic decay
length of the stress. Within the decay length, the stress is significant. Here $l=h/\beta$, $\beta$ is a coefficient related to the mismatch between the substrate and the film and $h$ is a uniform thickness of the film. In our experiments, the substrate is rigid compared with the film. Thus, in the case of uniform thickness, $\beta$ is about 0.8 [51]. Rearranging eq. (3), we have

$$d\sigma^d = \frac{dy}{\mathcal{T}}.$$  \hspace{1cm} (4)

and therefore the general solution of above differential equation is

$$\ln\sigma^d = -\frac{y}{l} + C,$$  \hspace{1cm} (5)

where $C$ is the integration constant. The in-plane stress vanishes on the crack surface $y=0$, where it requires $\Delta\sigma^d = \sigma^d$. Using this boundary condition, we can obtain the integration constant $C = \ln\sigma^d$. Thus, the released stress yields

$$\ln\frac{\sigma^d}{\sigma^d} = -\frac{y}{l},$$  \hspace{1cm} (6)

and an exponentially decaying stress distribution is

$$\sigma^d(y) = \sigma^d e^{-y/l}.$$  \hspace{1cm} (7)

The stress along the direction parallel to the crack is also released by the Poisson effect. Using the Hooke’s law, we can find

$$\Delta\sigma^d_p = c \Delta\sigma^d(y) = \sigma^d(1-e^{-y/l}),$$  \hspace{1cm} (8)

where $c$ is the Poisson’s ratio of the film. Hence, the in-plane stresses normal and parallel to the crack are [52]

$$\sigma^d_n = \sigma^d - \Delta\sigma^d_n(y) = \sigma^d(1-e^{-y/l}),$$  \hspace{1cm} (9)

$$\sigma^d_p = \sigma^d - \Delta\sigma^d_p(y) = \sigma^d(1-ve^{-y/l}).$$  \hspace{1cm} (10)

Near a crack tip, the variation of opening stress distributions can be described by $K_i$, and that of shearing stress distributions can be described by $K_\pi$. They are the stress intensity factors of mode I and mode II, respectively, and related with the energy release rate as $G = (K_i^2+K_\pi^2)/E'$, where $E' = E/(1-\nu^2)$ is the plane strain elastic modulus of the film and $E$ is the Young’s modulus of the film. It is difficult to calculate the energy release rate $G$ directly. Comparing the strain energy densities before and after cracking, one can finally find that the energy release rate is [51]

$$G = \frac{(\sigma^d)^2 h}{\beta E'} = \frac{(\sigma^d)^2 l}{E'},$$  \hspace{1cm} (11)

where the length scale is the film thickness, not the crack length [53]. As drying continues, the stress $\sigma^d$ increases. Then for the problem of crack propagation, the Griffith’s criterion is employed [54]. When the condition $G = G_c$ is satisfied, the crack grows. Here $G_c$ is a material parameter and denotes the critical energy release rate.

For the “daisy” pattern of an array of cracks, the average crack spacing along with the perimeter of the drying droplet $\lambda$ is discussed. For an array of cracks, the energy release rate $G$ per crack of the array is [55]

$$G = \frac{(\sigma^d)^2}{E'}\tanh\frac{\lambda}{2l}.$$  \hspace{1cm} (12)

For a brittle case, the wavelength $\lambda$ is proportional to the film thickness [56]. A possible explanation is that the flow of solvent away from a crack determines the crack spacing [57]. In our experiments, the dimensionless period $x_\lambda = \lambda/R_0$ normalized by the radius of the droplet $R_0$ was measured. The relationship between the dimensionless period and the dimensionless width of the coffee ring is shown in Figure 5(g), which indicates that $x_\lambda$ is not proportional to the width. On the contrary, a smaller spacing turns up when the width increases. Actually, the effects of the delamination and the plastic effects of the film make a difference to the spacing.

Moreover, as the deposition film dried further, the film was split into separated blocks in which spiral cracks were discovered. The blocks peeled off from the substrate, as a result, spiral cracks initiated at the edge of the blocks [25]. The colorful interference fringes indicated the peeling of the film (Figure 6(a)). The spiral cracks were triggered from the block edges and by defects, as shown in Figure 6(b). In addition to these single-spiral cracks, double-spiral cracks were observed in some blocks. They always rotated in the same direction in one block, as shown in Figure 6(c). Movie 3 gives the dynamic process of a spiral crack in the central part.

### 3.3.2 The “wavy-ring” pattern

The second category of crack pattern, i.e., the “wavy-ring” pattern, was acquired in drying droplets with low concentrations in our experiments. The critical concentrate was about 10‰–50‰. It is of great interest for its unique position and highly ordered shape. The periodically wavy cracks in the coffee ring render the “wavy-ring” pattern. In this category of crack pattern, there were two kinds of repeating templates of periodic cracks. One was saw-toothed, and the other was sinusoidal. The propagation process of a saw-toothed crack was observed in real time, as shown in Figure 7 (see Movie 4 for the dynamic propagation process). For a droplet with low concentration, the coffee ring took shape at first, followed by the formation of the central part in a few seconds with the droplets evaporating continuously. Then the cracks were triggered by defects where the stress concentrated, and propagated circularly in the coffee ring.

Compared with the growth of radial cracks under the humidity gradient of the whole film, the wavy-ring cracks take final shape in the coffee ring between two boundaries that fix the coffee ring to the substrate, as shown in Figure 8(a). For the coffee ring, the radius of the film is much larger com-
pared with the width of the coffee ring, so the curvature effect can be neglected. We assume that the coffee ring is a rectangular film under in-plane stress $\sigma$, as shown in Figure 8(b). Thus, the outer and inner boundaries are set at $y = \pm L/2$, and the thickness has

$$h = h_0 \cos \frac{ny}{2}, \quad \left( -\frac{L}{2} \leq y \leq \frac{L}{2} \right),$$

(13)

with $h_0$ the thickness of the centerline of the coffee ring and $L$ the width of the coffee ring. The varying thickness affects average in-plane stress, which finally determines the decay length of the stress. We take the two boundaries as two individual straight cracks to calculate the stress distribution in the coffee ring, and assume a uniform thickness $h$ and the decay length $l$. From eqs. (3)-(5), we find the released stresses of the outer and inner boundaries as

$$\ln \Delta \sigma_i^w = \frac{L}{2} - y + C_i, \quad \left( -\frac{L}{2} \leq y \leq \frac{L}{2} \right),$$

(14)

$$\ln \Delta \sigma_o^w = \frac{y + L}{2} + C_2, \quad \left( -\frac{L}{2} \leq y \leq \frac{L}{2} \right),$$

(15)

where $C_1$ and $C_2$ are the integration constants. Then the completely released stress by these two boundaries in the film is

$$\Delta \sigma^w = \Delta \sigma_0^w + \Delta \sigma_1^w.$$  

(16)

Considering the boundary conditions, $\Delta \sigma_i^w \big|_{y=\pm L/2} = \sigma^w$ and $\Delta \sigma_i^w \big|_{y=0} = \sigma_i^w \big|_{y=0}$, we obtain the integration constants as

$$C_1 = C_2 = \ln \frac{1 + e^{-\frac{L}{2}}}{1 + e^{-\frac{L}{2}}},$$

(17)

and the released stress as

$$\Delta \sigma^w = \sigma^w \frac{e^{\frac{L}{2}} + e^{-\frac{L}{2}}}{e^{\frac{L}{2}} + e^{-\frac{L}{2}}} = \sigma^w \frac{\cosh(y/L)}{\cosh(L/2L)}.$$  

(18)

Therefore, the stresses normal and parallel to the crack surface at the distance $y$ are

$$\sigma_n^w = \sigma^w - \Delta \sigma_n^w, \quad \sigma_p^w = \sigma^w - \nu \Delta \sigma_n^w.$$  

(19)

Using the stress distributions, we calculate the energy release rate of this crack as

$$G = \frac{h}{\beta E} \left[ (\sigma_n^w \cos \phi)^2 + (\sigma_p^w \sin \phi)^2 \right],$$

(20)

where $\phi$ denotes the angle to the $x$-axis and the weight function method is applied [59,60]. To achieve the maximum energy release rate, cracks in the coffee ring get wavy due to the oscillations of the stresses from the boundaries to the centerline. In the vicinity of boundaries, the stress components are primarily parallel to the bounding lines. Therefore, the middle crack curves to one side if it grows towards the boundaries. The film near the boundaries is thinner and stiffer, as a result, the location of maximum energy release rate will be at $\pm 90^\circ$ near the two boundaries. Thus, the crack deflects back to the centerline. Repetition of this process results in the “wavy-ring” pattern.

In a polar coordinate system $(r, \psi)$ with the origin at the center of the film, a sinusoidal-circular crack path in the “wavy-ring” pattern is geometrically described as

$$r = \frac{L}{2} \sin \frac{2\pi}{X_a} \psi + R_0 - \frac{L}{2} \psi,$$  

(21)

where $X_a$ is the dimensionless period, as shown in Figure 8(c). The relationship between the dimensionless width of the coffee ring $X_a$ and the dimensionless period of the “wavy-ring” pattern $X_a$ is

$$X_a \sim 2X_a,$$  

(22)

which indicates that the width of the coffee ring determines the periodicity of the “wavy-ring” crack pattern.
3.4 Relationship between the deposition film and the crack pattern

Certain parameters of the deposition patterns are used to quantify the conditions leading to each type of crack pattern. The dimensionless thickness $H$ is a function of the dimensionless width of the coffee ring $L$, which fits our experimental data as the following scaling law:

$$H = 0.6 \cdot L^{0.4}. \quad (23)$$

The above scaling law and the morphological diagram of crack patterns of drying protein droplets are shown in Figure 9. This graph is divided into four regions (Figure S1). In the first region ($H \sim 0$), drying droplets are deposited as typical coffee ring without any crack. Deposition film in this region is stable, since the thickness is too small to generate cracks. In the second region ($0 < H \leq 0.2$), the “wavy-ring” pattern forms in the coffee ring. In the third region ($0.2 < H \leq 0.55$), the “daisy” pattern shows up. The corresponding deposition film is also coffee ring. In this region, the minimum thickness of the central point exceeds a critical value, and numerous disordered cracks take shape in the center of the dried film. Meanwhile, spiral cracks are triggered in separated blocks. While in the last region ($H > 0.55$), to deposit a relatively uniform film, the concentration should be higher than 10%, which is that of the raw egg-white solution. Hence, the final crack pattern in the last region is not given.

4 Conclusions

Desiccation cracks and their patterns in drying droplets of protein solutions have been experimentally studied. We find that different drying processes cause different deposition and crack patterns. The experimental results reveal that the coffee-ring effect becomes more obvious as the concentration decreases. In addition, we identify two categories of crack patterns according to the position and shape of these arresting crack patterns, namely, “daisy” and “wavy-ring” patterns. We demonstrate that the “daisy” pattern appears in drying droplets with relatively high concentrations, whereas the “wavy-ring” pattern appears in drying droplets with low concentrations. Their formations and periodicities are explored. On one hand, the humidity gradient induces the radial crack propagation as the solvent evaporates. On the other hand, the coffee-ring effect tends to generate wavy cracks in the coffee ring. The relationship between the dimensionless width of the coffee ring and the dimensionless period of the “wavy-ring” pattern subjects to $\chi_\omega \sim 2 \chi_\omega$. The correlation between the deposition and the crack pattern is obtained. The deposition film is stable when the maximum thickness is too small to generate cracks. The “wavy-ring” crack pattern forms in the coffee ring as the thickness of the deposition...
film increases. When the minimum thickness of the central part exceeds a critical value, the “daisy” pattern arises. This study will help in understanding the formation mechanisms of crack patterns in drying droplets of protein solutions and assisting the future design of crack patterns in practical applications.

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Supporting Information

The supporting information is available online at tech.scichina.com and www.springerlink.com. The supporting materials are published as submitted, without typesetting or editing. The responsibility for scientific accuracy and content remains entirely with the authors. The supporting materials contain additional information about the experiments and results.
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