Evidence for $CP$ violation in $B^+ \to p\bar{p}K^+$ decays

The LHCb collaboration

Abstract

Three-body $B^+ \to p\bar{p}K^+$ and $B^+ \to p\bar{p}\pi^+$ decays are studied using a data sample corresponding to an integrated luminosity of 3.0 fb$^{-1}$ collected by the LHCb experiment in proton-proton collisions at center-of-mass energies of 7 and 8 TeV. Evidence of $CP$ violation in the $B^+ \to p\bar{p}K^+$ decay is found in regions of the phase space, representing the first measurement of this kind for a final state containing baryons. Measurements of the forward-backward asymmetry of the light meson in the $p\bar{p}$ rest frame yield $A_{FB}(p\bar{p}K^+, m_{p\bar{p}} < 2.85\text{ GeV}/c^2) = 0.495 \pm 0.012 \text{ (stat)} \pm 0.007 \text{ (syst)}$ and $A_{FB}(p\bar{p}\pi^+, m_{p\bar{p}} < 2.85\text{ GeV}/c^2) = -0.409 \pm 0.033 \text{ (stat)} \pm 0.006 \text{ (syst)}$. In addition, the branching fraction of the decay $B^+ \to \Lambda(1520)p$ is measured to be $B(B^+ \to \Lambda(1520)p) = (3.15 \pm 0.48 \text{ (stat)} \pm 0.07 \text{ (syst)} \pm 0.26 \text{ (BF)}) \times 10^{-7}$, where BF denotes the uncertainty on secondary branching fractions.

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Direct $CP$ violation can appear as a rate asymmetry in the decay of a particle and its $CP$ conjugate, and can be observed when at least two amplitudes, carrying different weak and strong phases, contribute to the final state. For $B$ mesons, it was observed for the first time in two-body $B^0 \rightarrow K^+\pi^-$ decays \cite{1,2}. The weak phases are sensitive to physics beyond the Standard Model that may appear at a high energy scale, and their extraction requires a determination of the relative strong phases. Three-body decays are an excellent laboratory for studying strong phases of interfering amplitudes. In particular, charmless decays of $B^+$ mesons, $B^+ \rightarrow K^+\pi^-\pi^+$, $B^+ \rightarrow K^+K^-K^+$, $B^+ \rightarrow \pi^+\pi^-\pi^+$, $B^+ \rightarrow K^+K^-\pi^+$ have been investigated recently \cite{3,5,7}. Similar studies have been conducted for the baryonic final states $B^+ \rightarrow p\bar{p}K^+$ and $B^+ \rightarrow p\bar{p}\pi^+$. In the $B^+ \rightarrow h^+h^-h^+$ decays ($h = \pi$ or $K$ throughout this Letter), large asymmetries, not necessarily associated to resonances, have been observed in the low $K^+K^-$ and $\pi^+\pi^-$ mass regions. These observations suggest that rescattering between $\pi^+\pi^-$ and $K^+K^-$ pairs may play an important role in the generation of the strong phase difference needed for $CP$ violation to occur \cite{7}. The $B^+ \rightarrow p\bar{p}h^+$ decays, although sharing the same quark-level diagrams, may exhibit different behavior due to the baryonic nature of two out of the three final-state particles.

This Letter reports the first evidence for $CP$ violation in charmless $B^+ \rightarrow p\bar{p}K^+$ decays. These decays are studied in the region with invariant mass $m_{p\bar{p}} < 2.85 \text{ GeV}/c^2$, below the charmonium resonances threshold. In addition, a more accurate measurement of the branching fraction of the decay $B^+ \rightarrow \bar{A}(1520)p$ is performed, using the reconstruction of $\bar{A}(1520) \rightarrow K^+\bar{p}$ decays, and improved determinations of the spectra and angular asymmetries are also reported. The mode $B^+ \rightarrow J/\psi(\rightarrow p\bar{p})K^+$ serves as a control channel. The data used have been collected with the LHCb detector and correspond to $1.0$ and $2.0 \text{ fb}^{-1}$ of integrated luminosity at $7$ and $8 \text{ TeV}$ center-of-mass energies in $pp$ collisions, respectively. The data samples are analyzed separately and the results are averaged.

The LHCb detector is a single-arm forward spectrometer covering the pseudorapidity range $2 < \eta < 5$, described in detail in Ref. \cite{8}. The detector allows for the reconstruction of both charged and neutral particles. For this analysis, the ring-imaging Cherenkov (RICH) detectors \cite{9}, distinguishing pions, kaons and protons, are particularly important.

The analysis uses simulated events generated by \textsc{Pythia} 8.1 \cite{10} with a specific LHCb configuration \cite{11}. Decays of hadronic particles are described by \textsc{EvtGen} \cite{12} in which final state radiation is generated using \textsc{Photos} \cite{13}. The interaction of the generated particles with the detector and its response are implemented using the \textsc{Geant4} toolkit \cite{14} as described in Ref. \cite{15}. Nonresonant $B^+ \rightarrow p\bar{p}h^+$ events are simulated, uniformly distributed in phase space, to study the variation of efficiencies across the Dalitz plane, as well as resonant modes such as $B^+ \rightarrow J/\psi(\rightarrow p\bar{p})K^+$, $B^+ \rightarrow \eta_c(\rightarrow p\bar{p})K^+$, $B^+ \rightarrow \psi(2S)(\rightarrow p\bar{p})K^+$, $B^+ \rightarrow \bar{A}(1520)(\rightarrow K^+\bar{p})p$, and $B^+ \rightarrow J/\psi(\rightarrow p\bar{p})\pi^+$.

Three charged particles are combined to form $B^+ \rightarrow p\bar{p}h^+$ decay candidates. The discrimination of signal from background is done through a multivariate analysis using a boosted decision tree (BDT) classifier \cite{17}. Input quantities include kinematical and

\footnote{Throughout the Letter, the inclusion of charge conjugate processes is implied, except in the definition of $CP$ asymmetries.}
Figure 1: Invariant mass distributions of (left) $p\bar{p}K^+$ and (right) $p\bar{p}\pi^+$ candidates. The points with error bars represent data. The solid black line represents the total fit function. The components are represented by blue dashed (signal), purple dotted (cross-feed), red long-dashed (combinatorial background) and green dashed-dotted (partially reconstructed background) curves.

topological variables related to the $B^+$ candidates and the individual tracks. The momentum, vertex and flight distance of the $B^+$ candidate are exploited, and track fit quality criteria, impact parameter and momentum information of final-state particles are also used. The BDT is trained using simulated signal events, and events in the high sideband of the $p\bar{p}h^+$ invariant mass ($5.4 < m(p\bar{p}h^+) < 5.5 \text{ GeV}/c^2$), which represent the background. Tight particle identification (PID) requirements are applied to reduce the combinatorial background and suppress the cross-feed between $p\bar{p}K^+$ and $p\bar{p}\pi^+$. The PID efficiencies are derived from calibration data samples of kinematically identified pions, kaons and protons originating from the decays $D^{*+} \to D^0(\to K^-\pi^+)\pi^+$ and $\Lambda \to p\pi^-$. 

Signal and background yields are extracted using unbinned extended maximum likelihood fits to the invariant mass distribution of the $p\bar{p}h^+$ combinations. The $B^+ \to p\bar{p}K^+$ signal is modeled by the sum of two Crystal Ball functions [18], for which the common mean and core width are allowed to float in the fit. Beside the signal component, the fit includes the parameterizations of the combinatorial background and partially reconstructed $B \to p\bar{p}K^*$ decays, where a pion from the $K^*$ decay is not reconstructed, resulting in a $p\bar{p}K$ invariant mass below the nominal $B$ mass. An asymmetric Gaussian function with power-law tails is used to model a possible $p\bar{p}\pi^+$ cross-feed component, where the pion is misidentified as a kaon. This contribution is found to be small.

The fit to the $B^+ \to p\bar{p}\pi^+$ decay uses similar parameterizations for the signal, combinatorial background, $p\bar{p}K^+$ cross-feed and partially reconstructed background from $B \to p\bar{p}\rho$ decays (with a missing pion from the $\rho$ decay). The cross-feed is found to be negligible.

The $B^+ \to p\bar{p}h^+$ invariant mass spectra are shown in Fig. 1. The signal yields obtained from the fits are $N(p\bar{p}K^{\pm}) = 18\,721 \pm 142$ and $N(p\bar{p}\pi^{\pm}) = 1988 \pm 74$, where the uncertainties are statistical only.

The distribution of events in the Dalitz plane, defined by $(m_{p\bar{p}}^2, m_{hp}^2)$ where $hp$ denotes the neutral combinations $h^-p$ and $h^+\bar{p}$, is examined. From the fits to the $B^+$ candidate
invariant mass, shown in Fig. 1, signal weights are calculated with the $sPlot$ technique \[19\]. These weights are corrected for trigger, reconstruction and selection efficiencies, which are estimated with simulated samples and calibration data. The Dalitz-plot variables are calculated constraining the $p\bar{p}h^+$ invariant mass to the known $B^+$ meson mass \[20\,21\]. Figure 2 shows the Dalitz distributions of the $B^+ \to p\bar{p}K^+$ events. Similarly to the results reported in Ref. \[6\,22\], clear signals of $J/\psi$, $\eta_c$ and $\psi(2S)$ resonances are observed, while $B^+ \to p\bar{p}K^+$ and $B^+ \to p\bar{p}\pi^+$ non-charmonium events both accumulate near the $p\bar{p}$ threshold. However, $B^+ \to p\bar{p}K^+$ events preferentially occupy the region with low $Kp$ invariant mass while $B^+ \to p\bar{p}\pi^+$ events populate the region with large $\pi p$ invariant mass. This difference in the Dalitz distribution can also be observed as a difference in the distribution of the helicity angle $\theta_p$ of the $p\bar{p}$ system, defined as the angle between the charged meson $h$ and the oppositely charged baryon in the rest frame of the $p\bar{p}$ system. The distributions of $\cos(\theta_p)$ are depicted in Fig. 3.

Data and simulation are used to assign systematic uncertainties, accounting for the
Figure 4: Forward-backward asymmetry in bins of $m_{p\bar{p}}$ for $B^+ \rightarrow p\bar{p}K^+$ and $B^+ \rightarrow p\bar{p}\pi^+$ decays. The data points are shown with their total uncertainties.

PID correction and fit model, to the angular and charge asymmetries, and to the relative branching fractions. The systematic uncertainty associated to the PID correction cancels in the asymmetry measurements.

The forward-backward asymmetry is measured as

$$A_{FB} = \frac{N_{pos} - N_{neg}}{N_{pos} + N_{neg}},$$

where $N_{pos}$ ($N_{neg}$) is the efficiency-corrected yield for $\cos \theta_p > 0$ ($\cos \theta_p < 0$). The obtained asymmetries are $A_{FB}(p\bar{p}K^+, m_{p\bar{p}} < 2.85 \text{ GeV}/c^2) = 0.495 \pm 0.012 \text{ (stat)} \pm 0.007 \text{ (syst)}$ and $A_{FB}(p\bar{p}\pi^+, m_{p\bar{p}} < 2.85 \text{ GeV}/c^2) = -0.409 \pm 0.033 \text{ (stat)} \pm 0.006 \text{ (syst)}$, where the systematic uncertainty is due to the ratio of average efficiencies in the regions $\cos \theta_p > 0$ and $\cos \theta_p < 0$. As reported in previous studies [6,23], the value for $B^+ \rightarrow p\bar{p}K^+$ contradicts the short-range analysis expectation [24].

The yields of the decays $B^+ \rightarrow p\bar{p}h^+$ in the region $m_{p\bar{p}} < 2.85 \text{ GeV}/c^2$ are obtained in the same way as for the integrated signals. Those of the resonant modes are extracted through two-dimensional extended unbinned maximum likelihood fits to invariant mass distributions of $p\bar{p}h^+$ and $p\bar{p}$ or $K^+\bar{p}$, using the same signal and background models for $m_{p\bar{p}}$ or $m_{K^+\bar{p}}$ as in Ref. [6]. The results are shown in Table 1. The branching fractions of the decays $B^+ \rightarrow \Lambda(1520)(\rightarrow K^+\bar{p})p$ and $B^+ \rightarrow p\bar{p}\pi^+$, $m_{p\bar{p}} < 2.85 \text{ GeV}/c^2$ are measured relative to the $J/\psi$ modes as

$$\frac{\mathcal{B}(B^+ \rightarrow \Lambda(1520)(\rightarrow K^+\bar{p})p)}{\mathcal{B}(B^+ \rightarrow J/\psi(\rightarrow p\bar{p})K^+)} = 0.033 \pm 0.005 \text{ (stat)} \pm 0.007 \text{ (syst)},$$

$$\frac{\mathcal{B}(B^+ \rightarrow p\bar{p}\pi^+, m_{p\bar{p}} < 2.85 \text{ GeV}/c^2)}{\mathcal{B}(B^+ \rightarrow J/\psi(\rightarrow p\bar{p})\pi^+)} = 12.0 \pm 1.2 \text{ (stat)} \pm 0.3 \text{ (syst)}.$$

The systematic uncertainties also include contributions from the background model. Using $\mathcal{B}(B^+ \rightarrow J/\psi K^+) = (1.016 \pm 0.033) \times 10^{-3}$, $\mathcal{B}(B^+ \rightarrow J/\psi\pi^+) = (4.1 \pm 0.4) \times 10^{-5}$,
The former measurement supersedes what is reported in Ref. [6]. Where BF denotes the uncertainty on the aforementioned secondary branching fractions.

A and accounting for the production and detection asymmetries. The raw asymmetry is corrected for acceptance, by taking into account the raw charge asymmetry is measured from the yields \(N\) as

\[
A_{\text{raw}} = \frac{N(B^- \to p\bar{p}h^-) - N(B^+ \to p\bar{p}h^+)}{N(B^- \to p\bar{p}h^-) + N(B^+ \to p\bar{p}h^+)}.
\]

and is investigated in the Dalitz plane using signal weights inferred from the fits shown in Fig. 1 for \(B^-\) and \(B^+\) samples. This asymmetry includes production and detection asymmetries. The statistics of the \(B^\pm \to p\bar{p}h^{\pm}\) decays is not sufficient to perform such an analysis, so only the \(B^\pm \to p\bar{p}K^{\pm}\) case is studied. An adaptative binning algorithm is used so that the sum of \(B^-\) and \(B^+\) events in each bin is approximately constant. Figure 5 shows the distribution of \(A_{\text{raw}}\) in the Dalitz plane. A clear pattern is observed near the \(\Delta \) threshold where \(A_{\text{raw}}\) is negative for \(m_{Kp}^2 < 10\text{ GeV}^2/c^4\) and positive for \(m_{Kp}^2 > 10\text{ GeV}^2/c^4\).

To quantify the effect, unbinned extended maximum likelihood simultaneous fits to \(B^-\) and \(B^+\) samples are performed in regions of the Dalitz plane, using the same models as the global fits. The raw asymmetry is corrected for acceptance, by taking into account the small difference in average efficiency due to the \(B^-\) and \(B^+\) samples populating differently the Dalitz plane. Physical asymmetries are obtained after acceptance correction (\(A_{\text{raw}}^{\text{acc}}\)) and accounting for the production \(A_{CP}(B^\pm)\) and kaon detection \(A_{\text{det}}(K^\pm)\) asymmetries:

\[
A_{CP} = A_{\text{raw}}^{\text{acc}} - A_P(B^\pm) - A_{\text{det}}(K^\pm).
\]

The decay \(B^\pm \to J/\psi(p\bar{p})K^\pm\), part of the selected sample, is used to determine \(A_\Delta = A_P(B^\pm) + A_{\text{det}}(K^\pm):\)

\[
A_\Delta = A_{\text{raw}}(B^\pm \to J/\psi(p\bar{p})K^\pm) - A_{CP}(B^\pm \to J/\psi K^\pm).
\]

Table 1: Event yields and selection efficiency for \(B^+ \to p\bar{p}K^+\) and \(B^+ \to p\bar{p}\pi^+\) final states.

| Mode | Yield | Efficiency (%) |
|------|-------|----------------|
| \(B^+ \to J/\psi(\to p\bar{p})K^+\) | 4260±67 | 1.55±0.02 |
| \(B^+ \to \eta_c(\to p\bar{p})K^+\) | 2182±64 | 1.47±0.02 |
| \(B^+ \to \psi(2S)(\to p\bar{p})K^+\) | 368±20 | 1.59±0.02 |
| \(B^+ \to \Lambda(1520)(\to K^+\bar{p})p\) | 128±20 | 1.39±0.01 |
| \(B^+ \to p\bar{p}K^+, m_{p\bar{p}} < 2.85\text{ GeV}/c^2\) | 8510±104 | 1.58±0.02 |
| \(B^+ \to J/\psi(\to p\bar{p})\pi^+\) | 122±12 | 1.07±0.01 |
| \(B^+ \to p\bar{p}\pi^+, m_{p\bar{p}} < 2.85\text{ GeV}/c^2\) | 1632±64 | 1.15±0.01 |

\(B(J/\psi \to p\bar{p}) = (2.17 \pm 0.07) \times 10^{-3}\), and \(B(\Lambda(1520) \to K^-p) = 0.234 \pm 0.016\), the branching fractions are measured to be:

\[
B(B^+ \to \Lambda(1520)p) = (3.15 \pm 0.48\text{ (stat)} \pm 0.07\text{ (syst)} \pm 0.26\text{ (BF)}) \times 10^{-7},
\]

\[
B(B^+ \to p\bar{p}\pi^+, m_{p\bar{p}} < 2.85\text{ GeV}/c^2) = (1.07 \pm 0.11\text{ (stat)} \pm 0.03\text{ (syst)} \pm 0.11\text{ (BF)}) \times 10^{-6},
\]

where BF denotes the uncertainty on the aforementioned secondary branching fractions. The former measurement supersedes what is reported in Ref. [6].

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Figure 5: Asymmetries of the number of signal events in bins of the Dalitz-plot variables for $B^\pm \to p\bar{p}K^\pm$. The number of events in each bin is approximately 300.

Figure 6: $N(B^-) - N(B^+)$ in bins of $m_{p\bar{p}}^2$ for $m_{Kp}^2 < 10\text{ GeV}^2/c^4$ (black filled circles) and $m_{Kp}^2 > 10\text{ GeV}^2/c^4$ (open triangles).

The value $A_{CP}(B^\pm \to J/\psi K^\pm) = (0.6 \pm 0.4)\%$ is taken from Ref. \[26\]. When using $A_{raw}(B^\pm \to J/\psi(p\bar{p})K^\pm)$, differences in the momentum asymmetry of the $p\bar{p}$ pair between $B^\pm \to J/\psi(p\bar{p})K^\pm$ and nonresonant $B^\pm \to p\bar{p}K^\pm$ decays are accounted for. A similar procedure is applied to obtain $A_{CP}(B^\pm \to J/\psi(2S)(p\bar{p})K^\pm)$ and $A_{CP}(B^\pm \to \eta_c(p\bar{p})K^\pm)$. The $B^\pm \to p\bar{p}\pi^\pm$ decays are also considered in the region $m_{p\bar{p}} < 2.85\text{ GeV}/c^2$. In this case, the correction also involves the pion detection asymmetry, $A'_{\Delta} = A_{raw}(B^\pm \to J/\psi(p\bar{p})K^\pm) - A_{CP}(B^\pm \to J/\psi K^\pm) - A_{det}(K^\pm) + A_{det}(\pi^\pm)$. The value $A_{det}(K^\pm) - A_{det}(\pi^\pm) = (-1.2 \pm 0.1)\%$ is taken from studies of prompt $D^+$ decays \[27\]. Table 2 shows the results, including asymmetries of resonant modes. Closer to the $p\bar{p}$ threshold enhancement, $m_{p\bar{p}}^2 < 6\text{ GeV}^2/c^4$, the asymmetry is found to reach the value $-0.066 \pm 0.026 \text{ (stat)} \pm 0.004 \text{ (syst)}$, for $m_{Kp}^2 < 10\text{ GeV}^2/c^4$. 
Table 2: CP asymmetries for $B^\pm \to p\bar{p}K^\pm$ and $B^\pm \to p\bar{p}\pi^\pm$ decays. The systematic uncertainties are dominated by the precision on the measurement $A_{CP}(B^\pm \to J/\psi K^\pm)$.

| Mode/region | $A_{CP}$ |
|-------------|----------|
| $\eta_c(p\bar{p})K^\pm$ | 0.040±0.034 (stat)±0.004 (syst) |
| $\psi'(2S)(p\bar{p})K^\pm$ | 0.092±0.058 (stat)±0.004 (syst) |
| $p\bar{p}K^\pm$, $m_{p\bar{p}} < 2.85$ GeV/c$^2$ | 0.021±0.020 (stat)±0.004 (syst) |
| $p\bar{p}K^\pm$, $m_{p\bar{p}} < 2.85$ GeV/c$^2$, $m_{Kp} < 10$ GeV$^2$/c$^4$ | -0.036±0.023 (stat)±0.004 (syst) |
| $p\bar{p}K^\pm$, $m_{p\bar{p}} < 2.85$ GeV/c$^2$, $m_{Kp} > 10$ GeV$^2$/c$^4$ | 0.096±0.024 (stat)±0.004 (syst) |
| $p\bar{p}\pi^\pm$, $m_{p\bar{p}} < 2.85$ GeV/c$^2$ | -0.041±0.039 (stat)±0.005 (syst) |

The systematic uncertainties are estimated by using alternative fit functions and splitting the data sample according to trigger requirements and magnet polarity. The overall systematic uncertainties are dominated by the uncertainty on the $A_{CP}(B^\pm \to J/\psi K^\pm)$ measurement.

In summary, an interesting sign-inversion pattern of the CP asymmetry appears at low $p\bar{p}$ invariant masses in $B^\pm \to p\bar{p}K^\pm$ decays. Although this resembles what is observed at low $h^+h^-$ masses in the $B^\pm \to h^+h^-h^-$ decays, the strong phase difference could involve a specific mechanism such as interfering long-range $p\bar{p}$ waves with different angular momenta \[24\]. In the region $m_{p\bar{p}} < 2.85$ GeV/c$^2$, $m_{Kp} > 10$ GeV$^2$/c$^4$, the measured asymmetry is positive with a significance of nearly 4$\sigma$, which represents the first evidence of CP violation in $b$-hadron decays with baryons in the final state. In the region $(m_{p\bar{p}}^2 < 6$ GeV$^2$/c$^4$, $m_{Kp}^2 < 10$ GeV$^2$/c$^4$), the asymmetry is negative with a significance of 2.5$\sigma$. The $h$ hadron forward-backward asymmetry in non-charmonium $B^+ \to p\bar{p}h^+$ decays is measured as $A_{FB}(p\bar{p}K^+, m_{p\bar{p}} < 2.85$ GeV/c$^2$) = 0.495±0.012 (stat)±0.007 (syst) and $A_{FB}(p\bar{p}\pi^+, m_{p\bar{p}} < 2.85$ GeV/c$^2$) = -0.409±0.033 (stat)±0.006 (syst). These asymmetries could be interpreted as being due to the dominance of nonresonant $p\bar{p}$ scattering \[24\]. Finally, an improved measurement of $B(B^+ \to \Lambda(1520)p) = (3.15 \pm 0.48$ (stat)±0.07 (syst)±0.26 (BF)) \times 10^{-7}$ is obtained.

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