We study the early stages of "central" pA and peripheral AA collisions. Several observables indicate that at a sufficiently large number of participant nucleons the system undergoes a transition into a new "explosive" regime. By defining a string-string interaction through the $\sigma$ meson exchange and performing molecular dynamics simulation, we argue that one should expect a strong collective implosion of the multi-string “spaghetti” state, creating significant compression of the system in the transverse plane. Another consequence is the collectivization of the “sigma clouds” of all strings into a chirally symmetric fireball. We find that these effects happen provided the number of strings $N_s > 30$ or so, as only such a number can compensate a small sigma-string coupling. These findings should help us to understand the subsequent explosive behavior, observed for the particle multiplicities roughly corresponding to this number of strings.

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I. INTRODUCTION

A. The evolving views on the high energy collisions

Before we get into our discussion of high-multiplicity pA collisions, let us start by briefly reviewing the current views on the two extremes: AA and minimum-bias pp collisions.

“Not-too-peripheral” AA we define as those which have the number of participant nucleons $N_p > 40$, and a corresponding multiplicity of the order of a few hundred. (Peripheral AA, complementary to this definition, we discuss in Sec. IV B.) Central AA collisions produce many thousands of secondaries: the corresponding fireball has an energy/entropy density well within the QGP domain, and these were naturally in the “mainstream” of the RHIC and LHC heavy-ion programs. Needless to say, the theory guidance and those experiments resulted in widely known conclusions about the strongly coupled dynamics of QGP. In particular, its collective flows were found to follow the hydrodynamical predictions with a remarkable accuracy.

(Hydrodynamical modeling typically starts at the proper time $\tau_i \sim 1/2$ fm, and the equation of state used is that of the fully equilibrated matter known from lattice simulations. The description of matter at earlier stages and the exact mechanism/degree of actual thermal equilibration are still a developing and hotly debated subject, which we do not address in this work.)

AdS/CFT correspondence provides a dual description of strongly interacting systems. In this vocabulary, the thermal fireball of deconfined matter is dual to a five-dimensional (5D) black hole, and its hydrodynamical expansion corresponds to the motion of this black hole off the space boundary (where the gauge theory is located). The attractively interacting and collapsing system of QCD strings we discuss should be viewed as a QCD analog to AdS/CFT black hole formation.

The opposite extreme is represented by typical (minimum bias) pp collisions. Its Pomeron description at a large impact parameter $b = 1 - 2$ fm is naturally given in terms of a double-string production (see Fig. 1 top). Color reconnection (described perturbatively or semiclassically, by a “tube” string diagram) leads to a pair of longitudinally stretched strings, with subsequent breaking into several pieces – hadronic clusters, which finally decay into a few final secondaries, as implemented in, e.g., the Lund model event generators, which do quite a good job in reproducing these phenomena. The density of a produced excitation is low, and it takes place in the confining QCD vacuum: thus the string description. The Pomeron profile, in particular, was historically the origin of the so-called $\alpha'(t = 0)$ parameter, related to the string tension, which defines the “string scale” both in QCD and in fundamental string theory.

(If collisions are “hard”, with a momentum transfer $Q \gg 1$ GeV, they resolve nucleons and Pomerons to their partonic substructure. The perturbative descrip-
tion of the Pomeron is well developed. At a very high density perturbative theory breaks down and may lead to the “color glass condensate” described by classical Yang-Mills fields. We, however, do not discuss hard collisions in this work, focusing instead on a soft string description.)

Both of these very different descriptions have reached sufficient maturity by now. The main question we discuss in this work is how they can be reconciled. In doing so, we address collisions which are intermediate between these two extremes. More specifically, one may ask where exactly the transition takes place and how sharp it is. It was argued that these two regimes are in fact separated by a third distinct regime similarly to the finite-temperature QCD, in which there is the so-called “mixed” phase between the confined (hadronic) and the deconfined (partonic) phases. As known from decades of theoretical and numerical (lattice) research, this is described most naturally by the near-critical strings, namely, strings in the Hagedorn regime. A similar transition has been found in the framework of the holographic Pomeron: here string fluctuations can be described by a thermal theory, with the effective temperature directly related to the impact parameter $b$. All three phases – the stringy one at large $b$, near-Hagedorn one at intermediate $b$, and (saturated) partonic one at small $b$ – can indeed be seen in the elastic scattering amplitude profile $F(b)$. However, this theory has so far been developed only for the tunneling (Euclidean) stage of the system: more work is needed to describe the subsequent evolution of the system and to relate these three regimes to the observations in the corresponding inelastic collisions.

In this paper, instead of challenging “central” (high multiplicity) pp collisions, we focus on simpler problems: (i) high-multiplicity pA and (ii) peripheral AA collisions. In both cases the cross sections used to be in the standard Pomeron regime (impact parameters as large as possible). So the number of participating nucleons $N_p$ and thus produced strings can be calculated from a known cross section by the standard Glauber-type calculation.

Yet if the number of involved participant nucleons is chosen to be large enough, $N_p = O(10)$, the emerging configuration resembles the “spaghetti” state shown in Fig. 1 (bottom). The system of strings, once produced by color exchanges as the target and projectile pass each other at $t \approx 0$, is then stretched longitudinally between the beams remnants, with large rapidities $+Y$ and $-Y$ comparable to those of the initial beams. As the generic rapidity interval is large, $\geq 10$, we focus on some intermediate $y$ between $-Y \ll y \ll Y$ (not close to the ends), where the collider detectors are. So one can view the set of strings as approximately parallel, directed along the beam direction.

We study conditions under which the strings are no longer independent from each other, and one has to take into account their interaction and the collective effects it may produce. As we describe in detail, these effects change from (i) the simple “spaghetti stage”, in which all strings are simply parallel and independent, to (ii) the situation in which strings start to move due to the influence of others, all the way to (iii) implosion into a localized cluster (or few clusters).

B. Explosive high multiplicity pp/pA collisions

The change in dynamics should lead to some visible changes in the observables. And indeed, as discovered at the LHC, low- and high-multiplicity pp/pA collisions show quite different behaviors. But before we discuss recent LHC experiments, let us briefly review the history of the subject.

The idea that a very small system produced in pp collisions, which can only be about $R_\perp \sim 1$ fm in its transverse size, can and should be treated hydrodynamically was first expressed by Landau in his pioneering 1953 paper. The road from this original idea to its realization turned out to be about 60 years long. Radial flow effects were searched for in minimum-bias pp collisions at CERN ISR more than 30 years ago by one of us [2], with negative results. The ISR spectra of identified $(\pi, K, \ldots)$ secondaries possessed the so-called “$M_1$-scaling”, consistent with independent string fragmentation and putting a rather stringent restriction on the possible magnitude of the collective flow. As we discuss below, minimally biased pp collisions do indeed produce a very dilute string system which provides no pressure gradient needed for an explosion.

In the 1990’s Bjorken suggested that one can look not at the typical (minimal-bias) pp collisions, but at a specially triggered high-multiplicity subset. Some indications for the radial flow in pp collisions at FERMILAB were found in higher multiplicity MINIMAX events [3]. Yet the magnitude of it remained inconclusive, the flow signal was weak, and we are unaware of any actual comparison between the hydro flow and the MINIMAX data.

With the advent of the LHC era of an extremely high luminosity and short-time detector capabilities, a hunt for strong fluctuations in the parton multiplicity became possible. Already during the very first run of the LHC in 2010, the CMS collaboration was able [4] to collect a sufficient sample of high-multiplicity pp collisions occurring with a probability of $\sim 10^{-6}$. CMS found the “ridge” correlation in the highest multiplicity bins, an angular correlation in the azimuthal angle between two particles at $\Delta y < 1$ which extends to a large rapidity range $|\Delta y| \geq 4$.

More recently the same phenomenon was seen in pPb collisions as well, now by the CMS [4], ALICE [5] and ATLAS [7] collaborations, as well as by PHENIX [6] in dAu collisions at RHIC. Larger number of “participant nucleons” and higher average multiplicity substantially weaken the cost of the trigger: the “ridge” is seen at the trigger level of a few percentages higher multiplicity events. It was shown that the ridge always comes with an “anti-ridge” on the other side of the azimuthal circle.
and is well described by the second and third harmonics of the azimuthal angle, very similar to that in peripheral AA collisions. These “elliptic” and “triangular” flows are characterized experimentally by the parameters \( v_n = \langle \cos(n\phi) \rangle, \ n = 2, 3 \).

The geometry of the initial state is different in \( pPb \) collisions at the LHC and \( dAu \) collisions at the RHIC: deuterons create “two-center explosions”, with an elliptic deformation \( \varepsilon_2 \) about twice as large [19]. The observed flow is also about twice as large: \( v_2^{dAu}/v_2^{pPb} \approx 2 \).

The radial flow in \( pA \) collisions was predicted [12] to be even larger than in AA. This was subsequently verified by the spectra of identified secondaries \( \pi, K \), and \( p, \Lambda \) by CMS and ALICE.

Recently the PHENIX \( dAu \) data set has been analyzed for the HBT radii [13]: their modulation with the elliptic flow \( v_2 \) direction, and radius-momentum correlations, further support the presence of strong radial and elliptic flows.

All those observations lead to the conclusions that Landau’s vision is perhaps realized in \( pA \) collisions, with \( P_{pA} \sim 10^{-2} \) probability in the highest multiplicity bins, and perhaps even in \( pp \), with the much lower probability \( P_{pp} \sim 10^{-6} \). The question is what exactly happens in those events, why they are different from the minimum-bias ones. This paper is an attempt to answer some of these questions.

Note that the very fact that such a small system with a radius of \( \sim 1 \) fm can behave macroscopically is not, by itself, so surprising. After all, the matter produced, known as sQGP, is approximately conformal. Its entropy density and viscosity scale as

\[
s \sim \eta \sim T^3
\]

so they do not have any scale of their own. So a small “conformal copy” of a large (\( AA \)) fireball should explode in exactly the same way. The problem is that, taken naively, these systems are not a “conformal copy”: their energy/entropy density is high, but not high enough. Hydro calculations using naive initial conditions underestimate the radial and elliptic flows.

A few comments on the pressure/entropy are in order. A QCD string (or a flux tube) is an object which, with parallel strings is not expected to produce transverse pressure: in fact we argue below that it, rather, has a tendency to implode. Therefore, in order to justify the observed explosive behavior of high-multiplicity events one needs to understand how a “spaghetti state” may turn itself into equilibrated QGP. The entropy issue is also related to this. If the hydrodynamical description of the explosion works (and it does), it tells us that basically the entropy is approximately conserved at this stage. So it must be there from the onset of the hydro stage. A “spaghetti state”, on the other hand, does not have a high entropy: thus some important changes must have occurred in between.

II. SETTING THE STAGE

A. A brief introduction to high multiplicity \( pA \)

It is by now well known that the multiplicity distribution in \( AA \) and \( pA \) collisions is mostly reproduced by the nuclear geometry and the so-called “wounded nucleon” model. It assumes that the final particle multiplicity (below characterized by the number of charged tracks \( N_{tr} \) seen by the CMS detector, with \( p_\perp > 0.4 \) GeV and in certain rapidity window) is generated via the distribution in the number of the so-called participant nucleons \( N_p \). Each participant nucleon is connected to the system by certain number of strings – 2 as a minimum – which fragment into secondaries independently. Furthermore, for simplicity, we assume that this decay process has a narrow (or zero) dispersion, or

\[
\frac{N_{tr}}{N_p} = \text{const}
\]

This simple one-parameter model is known to reproduce the multiplicity distribution in \( AA \) collisions. Glauber calculations for \( pA \) and \( dAu \) collisions allow us to calculate the distribution over \( N_p \) (see, e.g., those reported by Bozek [19]). One, in fact, does not need a detailed simulation to understand the main numbers involved. A nucleon hitting a heavy nucleus has a column of nuclear matter in front of it, which varies in size and density. The maximum obviously corresponds to the nuclear diameter \( 2R_A \) with a density approaching the saturated density of nuclear matter \( n_0 = 0.16 \text{ fm}^{-3} \). A tube with cross section \( \sigma \) contains an average number of nucleons

\[
\langle N_p \rangle = \sigma_{in} 2R_A n_0 \approx 20 ,
\]

where we have used the inelastic cross section at the LHC \( \sigma_{in} \approx 100 \text{ mb} = 10 \text{ fm}^2 \). Accounting for a realistic density distribution in nuclei, one gets a slightly reduced number,

\[
\langle N_p \rangle = 16 .
\]
Furthermore, if one ignores any correlations in nucleon positions (assumed in all Glauber studies we are aware of), the distribution in the number of participant nucleons $N_p$ should be described by a Poisson distribution with such an average.

In order to see if this simple model works for $pA$ collisions, we plotted as points the actual multiplicity distribution as measured by CMS (see Fig. 2). (In the CMS terminology, “tracks” are charged secondaries with $p_\perp > 0.4$ GeV in the rapidity coverage of their TPC tracker. The actual number of charged secondaries is about twice that number, and taking unobserved neutral secondaries into account the true multiplicity of secondaries produced is about a factor of 3 larger than the $N_{tr}$ used in this section.)

The curve in Fig. 2 is the Poisson distribution corresponding to the distribution over $N_p$ for a proton moving along the $Pb$ nucleus diameter; it does not describe the data. The left branch ($N_p < \langle N_p \rangle$) is in fact explained if a better account of the nuclear geometry – columns with fewer nucleons – is made (see, e.g., [11]). (His Figs. 2 an 3 use the highest multiplicity cutoff at the probability level of a few percent: specifically, $N_p > 18$, 4 percent centrality for $pPb$ and $N_p > 27$, 5 percent centrality for $dPb$.)

The right branch, with a larger multiplicity, $N_p > 80$, is different. All fluctuations in the positions of the nucleons are already included in the curve: apparently, it is not enough to explain the tail. Even if we relax the assumption of the zero-width decay of the strings and assign it a Poisson probability (still keeping the independence of the breaking processes), we will not describe the actual multiplicity pattern, which can be fitted by the negative binomial (NB) distribution (see, e.g., [11]), because the negative binomial distribution itself is not a convolution of two Poisson distributions. We think that the wounded nucleon model is inadequate, because for such multiplicities there are collective effects, described below.

The typical (inelastic) cross section of NN collisions at LHC energies is $\sigma_{\text{in}} \approx 10$ fm$^2$. The impact parameter in a collision is thus

$$b \sim \sqrt{\sigma_{\text{in}}/\pi} \approx 1.5 \text{ fm},$$

(5)

which is about 10 times the string radius $r_s \approx 0.15$ fm. The diluteness of our “spaghetti” state - the fraction of the volume occupied by $N_s$ strings – is then

$$\langle \text{diluteness} \rangle = N_s \left( \frac{r_s}{b} \right)^2 \approx 10^{-2} N_s.$$  

(6)

For a “minimally biased” (typical) collision producing just a few strings, it is indeed a rather dilute system. So, the independence of string fragmentation – assumed by the Lund model – seems to be reasonable. Even for $pA$ events corresponding to the heavy nucleus diameter, with $N_s \approx 30$, there seems to be enough space for all the strings, as the “diluteness” is only 0.3. And yet, as we show, there are good reasons to revisit the assumption of string independence.

### B. The onset of radial, elliptic and triangular flows

We do not review here any characteristics of the radial, elliptic, and triangular flows in most central $pA$ and peripheral $AA$, as done elsewhere. Let us just say that for the same multiplicity (or, perhaps, for the same “diluteness” [14]), they show striking similarities, which can be made even more precise using various scaling arguments, as in [14] and [16]. For the purposes of this paper we only need to localize the onset of all those phenomena.

**Radial flow** modifies the shapes of particle spectra differently, depending on their mass $M$. The data sets for identified secondaries $\pi, K, p$, and $\Lambda$ show a specific dependence on the particle mass of either (i) their mean transverse momentum $\langle p_\perp (M) \rangle$ or (ii) the $M_\perp$ distribution inverse slope $T'(M)$. The data (e.g., [17]) show no $M$ dependence for lower multiplicities, but the effect appears for higher ones, $N_{tr} > 80$.

**Elliptic flow** is, in these cases, measured also in two ways, by either the two-particle or the four-particle correlation parameters, $v_2\{2\}$ and $v_2\{4\}$. The latter one for $pA$ is especially sensitive to collectivity of the elliptic flow, and it has now been measured. It, however, rapidly drops below $N_{tr} \approx 80$ (see [14]). This is, perhaps, the best indicator for the onset of the explosive regime that we have so far. The $AA$ data for $N_{tr} < 80$ are too uncertain to see any trends there.

To summarize this subsection, there are at least three phenomena which seem to appear at about the same multiplicity (in the CMS definition, $N_{tr} > 80$), namely, (i) the radial and (ii) elliptic flows, as well as (iii) a multiplicity distribution extending well beyond that of the “wounded nucleon” model.

### III. COLLECTIVE STRING INTERACTIONS

#### A. Interaction in multi-string systems

Systems of many QCD strings have been studied since the early 1990’s in the context of Lund-like models of particle production.

The first discussed effect was the possibility of having overlapping strings, or string fusion, in which the color fields of the strings add up and result in a stronger field [18]. Decay of such objects, sometimes called “color ropes”, can enhance the production of strangeness and change $p_T$ spectra (see, e.g., [19] and subsequent literature). The strings did not interact with each other in the sense we employ in this paper.

As the number of strings and their density increase, they can be merged into larger clusters. The idea of color percolation was discussed in connection with deconfinement [20] and, also, strings [21]. When the diluteness of
strings reaches a certain critical value, the cluster takes over the whole system, which was suggested to become “deconfined” as a result. For a recent relation to high-multiplicity pp see also [22]. (These ideas are, in a way, complimentary to our treatment below, which focuses, however, on chiral symmetry restoration rather than deconfinement.)

Studies of the interaction of nonoverlapping strings have been done on the lattice, in a different setting. We do not go into this subject, because one can find a brief review of it in our previous paper [9].

Unlike that paper, here we consider not complicated string shapes, “string balls”, but a set of parallel and straight (unexcited) strings, called spaghetti. These strings have charges at the end, which move along the beam line, into positive and negative directions, with high rapidities. The equation of motion will be derived for a small segment of the string in the middle, of length δx. (The value of δx is irrelevant, as it appears both in the mass and in the force, and cancels out.) The calculation is done in the nonrelativistic approximation, assuming transverse string velocity v ≪ 1 and ignoring retardation effects. The string-string potential depends on mσr and, therefore, has an uncertainty in the sigma mass (due to its large decay width). This uncertainty is presumably larger than or comparable to the effect of retardation.

Following this, we assume the string interaction to be mediated by the lightest scalar σ. For one string the sigma “cloud” has a shape given by the quark condensate,

\[
\frac{\langle \bar{q}q(r_\perp)W \rangle}{(W')\langle \bar{q}q \rangle} = 1 - CK_0(m_\sigma \tilde{r}_\perp),
\]

(7)

where K_0 is the modified Bessel function and the “regularized” transverse distance \( \tilde{r}_\perp \) is

\[
\tilde{r}_\perp = \sqrt{r_\perp^2 + s_{\text{string}}^2},
\]

(8)

which smooths the two-dimensional (2D) Coulomb singularity ∼ ln(r_\perp) at small r_\perp. The parameter s_{\text{string}} is considered to be an “intrinsic” string width (in contrary to the effective string width, which is a result of quantum fluctuations).

Lattice simulations, such as [23], have found vacuum modifications due to the presence of a QCD string. We argued [9] that these data can be well described by a “sigma cloud” [7]. In Fig. 3 one can see our two-parameter fit to these data (the sigma mass here was taken to be m_σ = 600 MeV as an input, and was not fitted/modified). According to our fit, the intrinsic width is s_{\text{string}} ≈ 0.176 fm. After we had done the calculations, other lattice data [24] appeared, reporting the “intrinsic” width (penetration length of the dual superconductor picture in their case) to be equal to λ = 0.175 fm. Taken that our calculation was not supposed to be so precise, we treat this as an amazing match.

Since the strings are almost parallel to each other, the problem is reduced to the set of point particles on a plane with the 2D Yukawa interaction. From fit [7] one can see [9], that the main parameter of the string-string interaction (in string tension units) is numerically small,

\[
g_N\sigma_T = \frac{(\sigma)^2 C^2}{4\sigma_T} < 1,
\]

typically in the range \( 10^{-1} - 10^{-2} \). So, it is correctly neglected in situations for which the Lund model was originally invented – only when O(1) strings are created. The interaction starts to play a role when this smallness can be compensated by a large number of strings. As shown in Fig. 3 the magnitude of the quark condensate \( \sigma = |\langle \bar{q}q \rangle| \) at the string position is suppressed by about 20% of its vacuum value. So, in a “spaghetti” state one should think of the quark condensate suppression as being about 0.2 times the diluteness, [6], which is still < 1.

On the other hand, about 5 overlapping strings would be enough to eliminate the condensate and completely restore the chiral symmetry. If N_s > 30 strings implode into an area several times smaller than \( \sigma_{\text{in}} \), occur basically on top of each other and act coherently (which is the case as we will argue below), then the chiral condensate will be eliminated inside a region of 1 fm in radius, or about 3 fm\(^2\) in area. This will create a small hot QGP fireball.

Another possible approach to the flux tube interaction is developed within the Abelian Higgs (or dual superconductor) model of the QCD vacuum. In this picture the scalar field \( \phi \) is produced by the condensed magnetic monopoles. The vector (electromagnetic) field acquires mass due to the nonzero vacuum expectation value of the scalar field \( \langle \phi \rangle \neq 0 \). The ratio of the masses \( M_A/M_\phi \) defines the leading interaction channel between (and hence the sign of the interaction between) the Abrikosov flux tubes: if it is larger than 1, then one has domination of the attraction, i.e., a “type-I” superconductor. We assume that this is the case. There are also recent lattice data [24, 25] supporting our assumption in the SU(3) case.

![Fig. 3: (Color online) Normalized chiral condensate as a function of the radial coordinate transverse to the QCD string. Points are from the lattice data [24]. The curve is expression (7) with C = 0.26 and s_{\text{string}} = 0.176 fm.](image-url)
B. Other string phenomena

Although we study neither string breaking nor the excitation and annihilation of strings, we should comment on the parameters of these processes, since these will limit the time range of our description.

The longitudinally stretched strings in Fig. 1 (top) eventually break due to the so-called Schwinger-type mechanism of $q\bar{q}$ production in the electric flux tube. Without going into detail, we remind the reader that this implies an exponential suppression of string breaking. Its typical proper time,

$$\tau_{\text{breaking}} \sim 1 \text{ fm}/c,$$

may appear “normal”, but is, in fact, a long time in string units. The clusters produced in the process of string breaking have a length of about $l_{\text{breaking}} \sim 2 \text{ fm}$, which is indeed large in comparison to the string radius of only about 0.15 fm. A typical mass of the string segments is $M_{\text{breaking}} \sim \sigma T \cdot l_{\text{breaking}} \sim 2 \text{ GeV}$, so these are not hadrons but “stringy clusters”, decaying into or for five pions later.

After breaking, the string enters the so-called yo-yo stage, in which the quark and antiquark at the string ends are accelerated towards each other by the string tension. The effective transverse mass of a quark is $m_{\perp} = \sqrt{m^2 + p_T^2} \sim 1/2 \text{ GeV}$, while the string tension is $\sigma T \approx 1 \text{ GeV/fm}$; thus, the effective quark acceleration $a_{\perp} \sim 2 \text{ fm}^{-1}$. The quark rapidity changes as

$$y = a_{\perp} \tau,$$

and this process happens from both ends of the string pieces, each about 2 units of rapidity long. Therefore, the strings shrink and disappear within a time $\tau_{\text{yoyo}} \sim 0.5 \text{ fm}/c$. Their sum,

$$\tau_{\text{breaking}} + \tau_{\text{yoyo}} \approx 1.5 \text{ fm}/c,$$

is naturally a limit of the time which is available for the collective string effects we study.

The presence of many strings of the same color and opposite color fluxes may induce another dissipative phenomenon, namely, flux-antiflux annihilation. It is also suppressed, not exponentially, but only by $N_c$. If this happens, then the strings are reconnected as shown:

$$\Rightarrow \quad \left( \begin{array}{c} \text{---} \\ \text{---} \end{array} \right) \quad \text{---} \quad \left( \begin{array}{c} \text{---} \\ \text{---} \end{array} \right).$$

Longitudinal tension of the string forces the connecting part – we refer to it as the “zipper” – to move longitudinally. If it is made of a semicircular string piece with diameter $d$, then its acceleration is

$$a_{\parallel} = \frac{4}{\pi d},$$

and the relativistic motion with such acceleration in terms of rapidity and proper time is simply given by

$$y_{\text{zipper}} = a_{\parallel} \tau.$$

Since $\tau < \tau_{\text{breaking}}$ and $d \sim 1 \text{ fm} \sim \tau_{\text{breaking}}$, one finds that a zipper can only move by about 1 unit of rapidity during the time considered, of the total rapidity interval $2Y \sim 10$. We thus conclude that there is no enough time to “unzip” the string system.

C. Mean field

Assuming cylindrical symmetry, one can get the shape of the mean sigma distribution by solving the radial equation on the sigma field. We write it as

$$\sigma''(r_\perp) + \frac{1}{r_\perp} \sigma'(r_\perp) - m_\sigma^2 \sigma(r_\perp) = \rho(r_\perp),$$

where $\rho(r_\perp)$ is the matter distribution in the transverse space. Note that we have not included the coupling constant on the right-hand side or any normalization factors: this can be simply incorporated into the solution once it is known, since Eq. (16) is linear. We use, for example, a Gaussian source, $\rho = \exp[-r_\perp^2/(2R^2)]$.

At large distances the right-hand side of (16) is negligibly small, and the solution has the form

$$\sigma(r_\perp) = C \cdot K_0(m_\sigma r_\perp),$$

which can be used to fix asymptotics of the numerical solution at large $r$. If the integration is performed starting from a large $r$ downwards, then the generic solution blows up at small $r$, unless the constant $C$ is specially tuned. In Fig. 4 we show two such solutions, with tuned constants $C = 3757.21$ and $42.37$ and radii $R = 1.5$ and 0.7 fm, respectively (the solutions are rescaled in the plot, so that the integral of the source is normalized to 1). These two radii are supposed to exemplify the “spaghetti” transverse size before and after a collapse: as one can see from the figure, the depth of the sigma potential well increases roughly by a factor of 5 between these two cases. This is more than enough to completely cancel chiral symmetry breaking around the after-collapse system.
FIG. 5: (Color online). The (dimensionless) kinetic energy (upper curve) and potential energy (lower curve) of the system for the same example as shown in Fig. 7 as a function of time \( t \) (fm/c). The horizontal line with points is their sum, \( E_{\text{tot}} \), which is conserved.

FIG. 6: (Color online). Kinetic energy (dimensionless) versus the simulation time (fm/c), for few \( pA \) runs with \( N_s = 50 \). The seven curves (bottom-to-top) correspond to increasing coupling constants \( g_N \sigma_T = 0.01, 0.02, 0.03, 0.05, 0.08, 0.10, \) and 0.20. The shaded region at the right corresponds to the time which is considered to be too late for strings to exist, due to their breaking.

**IV. MOLECULAR DYNAMICS STUDY**

**A. Initialization for central \( pA \) and peripheral \( AA \)**

To simulate central \( pA \) we first select the number of participant (or “wounded”) nucleons \( N_p \) = 5, 10, 15, 20, and 25 and select their random positions in the transverse plane. The numbers correspond to \( p \) moving along the diameter of \( Pb \) as discussed above, while variation in the number roughly corresponds to expected fluctuations.

The azimuthal angle is random, with the uniform distribution. The distance from the origin, \( b \) (i.e., the center of the original proton), is taken with the weight given by the elastic scattering amplitude profile:

\[
dP = F(b) \, \sigma \, db.
\]  

(18)

We used the profile function from the Bourrely-Soffer-Wu (BSW) model [26] [see their expressions (13-15)], which fitted well to the LHC data. Because the profile function is flat, \( F(b) \approx 1 \) for \( b < 0.4 \) fm, the density of strings is approximately constant at the center. The corresponding initial energy density in this region,

\[
\epsilon_0 = \sigma_T n_s, \tag{19}
\]

ranges from about \( \epsilon_0 = 2 \) to 9 GeV/fm\(^3\). The lower value, if equilibrated, would belong to the mixed phase. The upper value is inside the QGP domain, but barely. So, even if equilibration of this state happened, one would not expect a hydro explosion, as its equation of state is quite soft. As we show below, collective string effects could increase these numbers by roughly an order of magnitude and, thus, change the conclusion.

Peripheral \( AA \) are modeled in the standard Glauber way, except that we take the number of participants being in exactly the same bins, namely, \( N_p = 5, 10, 15, 20, \) and 25, for comparison.

**B. Peripheral \( AA \)**

Let us briefly describe how we choose the initial string configurations in this case. The relation between the impact parameter of two nuclei \( b_{AA} \) and the number of participant nucleons \( N_p \) is given by the standard Glauber simulation, with \( \sigma_{tot} = 120 \) mb. We then select bins with a certain number of \( N_p \), and pick out several random events from an ensemble. These are evolved using the molecular dynamics code.

The Pomeron undergoes a tunneling (Euclidean) stage, from which it appears as two strings (with opposite color fluxes). At time \( t=0 \) the strings are transverse to the beam, with their length given by the impact parameters between nucleons \( b_{NN} \). The strings are also separated in the transverse plane by

\[
\delta_{x_{\perp}} = \frac{\pi}{T_{eff}}, \tag{20}
\]

where \( T_{eff} \) is the effective temperature introduced in [8]. While, in principle, it depends on \( b_{NN} \) and the logarithm of the collision energy, we did not include these dependencies and use a randomly oriented vector of length 0.2 fm.

Since the end points of each string are at large rapidities \( \sim \pm Y_{c} \), at \( t > 0 \) strings interpolate linearly between these points. Since most measurements are done at midrapidity, the transverse location of the string is at the midpoint between the two nucleons. Thus we do not need to model \( b_{NN} \) and its distribution.

**C. Time evolution**

As discussed above, the strings can be viewed as a 2D gas of particles (in the transverse plane) with unit masses and \( \epsilon_{ij} \). The forces between them are given by the derivative of the energy, [7], and so

\[
\vec{r}_{ij} = \vec{f}_{ij} = \frac{\vec{r}_{ij}}{r_{ij}} (g_N \sigma_T) m_\sigma 2K_1(m_\sigma \vec{r}_{ij}). \tag{21}
\]
FIG. 7: (Color online) Example of changing transverse positions of the 50 string set: the four plots correspond to one initial configuration evolved to times $\tau = 0.1, 0.5, 1,$ and $1.5\text{ fm/c}$. Distances are given in femtometers, and $g_N\sigma_T = 0.2$.

FIG. 8: (Color online) Example of peripheral AA collisions, with $b = 11\text{ fm}$, $g_N\sigma_T = 0.2$, and the 50-string set. The four plots of the string transverse positions $x, y (\text{fm})$ correspond to times $\tau = 0.1, 0.5, 1.,$ and $2.6\text{ fm/c}$.

FIG. 9: (Color online) The left plot is for central $pA$, the right one – for peripheral AA collisions. The vertical axis is the effective coupling constant $g_N\sigma_T$ (dimensionless). The horizontal axis is the maximal energy density $\epsilon_{\text{max}}$ (GeV/fm$^3$) defined by the procedure explained in the text. Five sets shown by different symbols correspond to string number $N_s = 10, 20, 30, 40, 50$, left to right respectively.

In our simulations we used a classical molecular dynamics code based on the double-precision CERNLIB solver DDEQMR. In Figs. 7 and 8 we show an example of one particular configuration with $N_s = 40$. In order to study a longer time evolution, we took a somewhat larger coupling, $g_N\sigma_T = 0.2$. As shown in Fig. 7,

the conservation of the (dimensionless) total energy

$$E_{\text{tot}} = \sum_i \frac{v_i^2}{2} - 2g_N\sigma_T \sum_{i>j} K_0(m_\sigma r_{ij})$$

is indeed observed: its accuracy is about $10^{-4}$. An even higher accuracy is observed for the total momentum (which remains 0).

The evolution consists of two qualitatively distinct parts: (i) early implosion, which converts the potential energy into the kinetic one, which has its peak when a
fraction of the particles “gravitationally collapses” into a tight cluster; and (ii) subsequent approach to a “mini-
galaxy” in virial quasi-equilibrium. To illustrate better
the first stage of the motion we took a number of screen-
shots: a typical case is shown in Fig. T. Starting from vari-
ous initial configurations we occasionally see more com-
licated scenarios realized, e.g., two minigalaxies flying
away from each other.

One can see that the total kinetic energy shows a peak
and then oscillates. Its average over time approaches
some mean value, which of course should be related to the
“virial” value

\[ 2\langle E_{\text{kin}} \rangle = \left( \sum_i r_i \frac{\partial U}{\partial r_i} \right) \]  

(23)
as time goes to infinity. (This is the standard outcome of
molecular dynamics studies, e.g., stars in galaxies have a
similar quasi-equilibrium).

Simulations for peripheral AA show a particular fea-
ture. As exemplified in Fig. S the initial strong deforma-
tion of the system – its y-direction size is much larger
than that in the x direction – the collapse occurs in two
stages. First, one observes a rapid 1D collapse along the
x axes, followed by a much slower collapse along the y di-
rection. If the simulation runs long enough, the resulting
cluster becomes, of course, isotropic.

D. Results

We simulated similar time evolutions for ensembles of
randomly generated initial conditions. Systematic re-
results were organized as follows. We have ensembles of
10 independent runs for each set of parameters, string
numbers \( N_s = 10, 20, 30, 40, \) and 50, coupling constants
\( g N \sigma_T = 0.01, 0.02, 0.03, 0.05, 0.08, 0.1, \) and 0.2, and two
different initializations, corresponding to the central \( pA \)
and peripheral AA cases.

The dependence of the evolution timescale on the value
of the coupling is shown in Fig. T. While the value it-
self grows substantially with the coupling, the “implosion
time” (the location of the first peak) depends on the cou-
pling more gradually.

Of the many possible observables we selected the lo-
cal density in the generated clusters \( \epsilon_{\text{max}} \) defined by the
following procedure. As the first step, we find the loca-
tion of the most rapidly moving particle, resembling early
searches for the location of the black hole at our galaxy
center. After it is found, its position is taken as the clus-
ter center, and the number of particles inside the circle
of fixed radius \( r_0 = 0.3 \) fm is used to calculate the max-
imal 2D density \( n_{\text{max}} \). The results are converted to the
maximal energy density of a run by

\[ \epsilon_{\text{max}} = \sigma_T n_{\text{max}} \]  

(24)and averaged over the runs.

The output is shown in Fig. T as the maximal energy
density reached (during the proper time \( \tau < 2 \) fm/c).
The main result is that the implosion of the system pro-
duces values which are significantly higher than those at
the initial time \( \tau = 0 \), namely \( \epsilon_0 = 2 \) to 9 GeV/fm³ for
these sets.

While the rate of evolution depends on the strength
of the coupling, the maximal energy density reached is
much less sensitive to it. As one can see from this, for a
small number of strings, \( \sim 10 \), there is no dependence on
the coupling in the range selected: these are too small to
create any effect. However, as \( N_s > 30 \), the coupling be-
comes important: it increases the density by a significant
factor, reaching values as large as \( \epsilon_{\text{max}} \sim 80 \) GeV/fm³.

As such a high energy density is being reached, the
string description of the system can no longer be main-
tained. The kinetic energy is transferred into multiple
string states, and the strings become highly excited. If
the system fully equilibrated into the sQGP, the temper-
ature would be about \( T_f \sim 500 \) MeV \( \sim 3 T_c \), enough to
generate a very robust hydro explosion.

Finally, in Fig. T we show an example of the instanta-
aneous collective potential produced by the strings in the
transverse plane. The white regions correspond to poten-
tial values smaller than \( -5 \cdot 2 g N \sigma_T (\text{fm}^{-1}) \approx -400 \) MeV;
i.e., chiral symmetry can be completely restored in these
regions. A large gradient of this potential at its edge can
cause quark pair production, similar to the Schwinger
process in an electric field: one particle may flow out-
ward and one fall into the well. This phenomenon is a
QCD analog to Hawking radiation at the black hole hori-
zon. An analogous picture was also considered in [27] and
[28]. The final ellipticity of the induced elliptic flow will
be studied elsewhere.

FIG. 10: (Color online) Instantaneous collective potential
(in units of \( 2 g N \sigma_T \)) for an AA configuration with
\( b = 11 \) fm, 
\( g N \sigma_T = 0.2, N_s = 50 \) at the moment in time
\( \tau = 1 \) fm/c. White regions correspond to the chirally restored phase.
V. SUMMARY AND OUTLOOK

In this work we have discussed collective interactions between QCD strings in a “spaghetti” configuration, created in “central” pA and peripheral AA collisions. We first provided an experimental overview, concluding that at least three observables – multiplicity distribution, radial flow and elliptic flow – show the onset of a different regime at the string number $N_s \sim 30$. Although this number may appear to be large, one can see that, naively, the produced system remains sufficiently dilute. In particular, under this condition the chiral condensate should be somehow analogous to the universal Bekenstein entropy produced in multistring annihilation/excitation QCD analog to Hawking radiation. And the amount of entropy produced in multistring annihilation/excitation should be somehow analogous to the universal Bekenstein entropy of a black hole.

One may argue that the string description must break down, as the string density (and hence the energy density of the system) is increased by a significant factor due to the implosion. It is expected that it undergoes a rapid equilibration into the QGP phase, which then explodes the implosion. It is expected that it undergoes a rapid equilibration into the QGP phase, which then explodes.

If so, the holographic framework uniquely connects the collective sigma field displayed in Fig. 4 should presumably lead to the particle pair production at its edge – the QCD analog to Hawking radiation. And the amount of entropy produced in multistring annihilation/excitation should be somehow analogous to the universal Bekenstein entropy of a black hole.

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