World Ocean Thermocline Weakening and Isothermal Layer Warming

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Abstract: This paper identifies world thermocline weakening and provides an improved estimate of upper ocean warming through replacement of the upper layer with the fixed depth range by the isothermal layer, because the upper ocean isothermal layer (as a whole) exchanges heat with the atmosphere and the deep layer. Thermocline gradient, heat flux across the air–ocean interface, and horizontal heat advection determine the heat stored in the isothermal layer. Among the three processes, the effect of the thermocline gradient clearly shows up when we use the isothermal layer heat content, but it is otherwise when we use the heat content with the fixed depth ranges such as 0–300 m, 0–400 m, 0–700 m, 0–750 m, and 0–2000 m. A strong thermocline gradient exhibits the downward heat transfer from the isothermal layer (non-polar regions), makes the isothermal layer thin, and causes less heat to be stored in it. On the other hand, a weak thermocline gradient makes the isothermal layer thick, and causes more heat to be stored in it. In addition, the uncertainty in estimating upper ocean heat content and warming trends using uncertain fixed depth ranges (0–300 m, 0–400 m, 0–700 m, 0–750 m, or 0–2000 m) will be eliminated by using the isothermal layer. The isothermal layer heat content with the monthly climatology removed (i.e., relative isothermal layer heat content) is calculated for an individual observed temperature profile from three open datasets. The calculated 1,111,647 pairs of (thermocline gradient, relative isothermal layer heat content) worldwide show long-term decreasing of the thermocline gradient and increasing of isothermal layer heat content in the global as well as regional oceans. The global ocean thermocline weakening rate is \((-2.11 \pm 0.31) \times 10^{-3} \,(\degree\text{C}\,\text{m}^{-1}\,\text{yr}^{-1})\) and isothermal layer warming rate is \((0.142 \pm 0.014)\,\text{W}\,\text{m}^{-2}\).

Keywords: isothermal layer; thermocline; isothermal layer heat content; isothermal layer warming; thermocline gradient; thermocline weakening

1. Introduction

The thermocline with a strong vertical gradient is the transition layer between the vertically quasi-uniform layer from the surface, the isothermal layer (ITL), and the deep-water layer [1,2]. Intense turbulent mixing near the ocean surface causes formation of ITL. The thermocline resists the turbulent mixing from the ITL and limits the ITL deepening and heat exchange between the ITL and deeper layer due to its strong vertical gradient. The mean thermocline gradient \((G)\) directly affects the ITL warming or cooling [3–6].

The oceanic climate change is represented by temporal variation of the upper layer ocean heat content (OHC), which is the integrated heat stored in the layer from the sea surface \((z = 0)\) down to a below-surface depth. Here, \(z\) is the vertical coordinate. The below-surface depth can be either a fixed depth or the ITL depth \((h)\). With \(h\) as the below-surface depth, the upper layer OHC is called the ITL heat content \((H_{ITL})\). Both \(G\) and \(H_{ITL}\) are important in ocean prediction [6].
However, the oceanographic community uses various fixed depths to define the OHC such as 0–300 m \[7,8\], 0–400 m \[9\], 0–700 m \[10,11\], 0–750 m \[12\], 0–2000 m \[13\], deep layer OHC such as below 700 m \[8\], and below 2000 m \[14\], and the full layer OHC \[15\]. We apologize for not citing all the work on the ocean OHC due to the huge amount of literature. Interested readers are referred to two excellent review papers \[16,17\].

Such fixed-depth OHC has three weaknesses. First, the layer with the fixed depth range includes ITL, the thermocline, and the layer below the thermocline. The effects of the thermocline gradient on ocean climate change and phytoplankton dynamics are not represented. Phytoplankton growth depends upon water temperature, light, and availability of nutrients. Nutrients are normally brought up from deep waters and into the photic zone where phytoplankton growth can occur \[18\]. Such nutrient pumping is affected by the thermocline gradient. Second, the fixed-depth OHC leads to the uncertainty in estimating the upper ocean warming trend. For example, the warming trend is estimated as 0.64 ± 0.11 W m\(^{-2}\) for OHC (0–300 m) on 1993–2008 with the significant level \(\alpha = 0.10\) \[8\], 0.26 ± 0.02 W m\(^{-2}\) for OHC (0–300 m) on 1975–2009 \[14\] and 0.20 W m\(^{-2}\) for OHC (0–700 m) on 1955–2012 \[10\], among others (see Table 1). Third, there is no simple relationship between the OHC with the fixed depth range and the sea surface temperature, which is the most important oceanic variable for the heat exchange between the ocean and atmosphere.

Table 1. Several reported trends (warming rate) of fixed depth ocean heat content anomaly.

| Source | Fixed-Depth Layer | Trend (W m\(^{-2}\)) | Duration |
|--------|------------------|----------------------|----------|
| Lyman and Johnson (2014) \[11\] | \(H_{0-100\ m}\) | 0.07 | 1956–2011 |
| Lyman and Johnson (2014) \[11\] | \(H_{0-100\ m}\) | 0.10 | 1967–2011 |
| Lyman and Johnson (2014) \[11\] | \(H_{0-100\ m}\) | 0.09 | 1983–2011 |
| Lyman and Johnson (2014) \[11\] | \(H_{0-100\ m}\) | \(-0.04\) | 2004–2011 |
| Lyman et al. (2010) \[8\] | \(H_{0-300\ m}\) | 0.64 ± 0.11 | 1993–2008 |
| Lyman and Johnson (2014) \[11\] | \(H_{0-300\ m}\) | 0.19 | 1967–2011 |
| Lyman and Johnson (2014) \[11\] | \(H_{0-300\ m}\) | 0.25 | 1983–2011 |
| Lyman and Johnson (2014) \[11\] | \(H_{0-300\ m}\) | 0.10 | 2004–2011 |
| Balmaseda et al. (2013) \[14\] | \(H_{0-300\ m}\) | 0.26 ± 0.02 | 1975–2009 |
| Balmaseda et al. (2013) \[14\] | \(H_{0-700\ m}\) | 0.38 ± 0.03 | 1975–2009 |
| Levitus et al. (2012) \[10\] | \(H_{0-700\ m}\) | 0.27 | 1955–2010 |
| Lyman and Johnson (2014) \[11\] | \(H_{0-700\ m}\) | 0.43 | 1983–2011 |
| Lyman and Johnson (2014) \[11\] | \(H_{0-700\ m}\) | 0.13 | 2004–2011 |
| Willis et al. (2003) \[12\] | \(H_{0-750\ m}\) | 0.86 ± 0.12 | 1993–2003 |
| Lyman and Johnson (2014) \[11\] | \(H_{0-1800\ m}\) | 0.29 | 2004–2011 |
| Levitus et al. (2012) \[10\] | \(H_{0-2000\ m}\) | 0.39 | 1955–2010 |
| Zanna et al. (2019) \[13\] | \(H_{0-2000\ m}\) | 0.30 ± 0.6 | 1955–2017 |

Alternatively, we use the ITL OHC (\(H_{ITL}\)) to overcome these three weaknesses of the traditional OHC with the fixed depth range. Recently, a global ocean synoptic thermocline gradient (\(G\)) and isothermal layer depth (\(h\)) dataset has been established from the NOAA/NCEI World Ocean Database (WOD) with each (\(G, h\)) pair corresponding to particular CTD (or XBT) temperature profile in WOD \[19,20\]. This synoptic dataset is at the NOAA website (https://www.ncei.noaa.gov/access/metadata/landing-age/bin/iso?id=gov.noaa.nodc:0173210) for public use. With the given ITL depth \(h\), it is easy to compute ITL heat content (\(H_{ITL}\)). After the quality control, we have 1,111,647 (\(G, H_{ITL}\)) data pairs for the global oceans. The warming trend can be identified from the \(H_{ITL}\) data. A new phenomenon ‘thermocline weakening’ was explored.

2. Data

Three open datasets were used for this study. The first one is the NOAA World Ocean Database 2018 (WOD18) conductivity, temperature, depth (CTD) and expendable bathythermograph (XBT) temperature profiles \(T(t, r, z)\) 1970–2017 (https://www.nodc.noaa.gov/OC5/WOD/pr_wod.html) \[19\].
Here, the Earth coordinate system is used with \( r = (x, y) \) for the longitudinal and latitudinal and \( z \) in the vertical (upward positive). The second one is the 0.25° × 0.25° gridded climatological monthly mean temperature fields \( T_c(t_c, r_c, z_c) \) of the NOAA World Ocean Atlas 2018 (WOA18) (https://www.nodc.noaa.gov/OC5/woa18/) [20] with \( t_c \) representing the month, \( r_c \) the horizontal grid point, and \( z_c \) the WOA standard depth. The third one is the global ocean thermocline gradient, ITL depth, and other upper ocean parameters calculated from WOD CTD and XBT temperature profiles from 1 January1970 to 31 December 2017 (NCEI Accession 0173210) (https://data.nodc.noaa.gov/cgi-bin/isoid=gov.noaa.nodc:0173210) [21], which was established using the optimal schemes [22–24]. The third dataset contains 1,202,061 synoptic \( G(t, r) \) and \( h(t, r) \) for the world oceans [25]. Each data pair has a corresponding observed temperature profile \( T(t, r, z) \) in the first dataset.

The decadal variations of statistical parameters for the global \((G, h)\) data are depicted in Table 2 (isothermal layer depth \( h \)) and Table 3 (thermocline gradient \( G \)). Both \((h, G)\) are positively skewed. The isothermal layer depth \( h \) monotonically increased its mean (standard deviation) from 38.8 m (41.7 m) during 1970–1980 to 67.5 m (61.7 m) during 2011–2017, and monotonically decreased skewness (kurtosis) from 3.97 (27.3) during 1970–1980 to 2.70 (15.1) during 2011–2017. The thermocline gradient \( G \) monotonically decreased its mean (standard deviation) from 0.204 °C/m (0.167 °C/m) during 1970–1980 to 0.121 °C/m (0.134 °C/m) during 2011–2017, and increased its skewness (kurtosis) from 1.35 (5.02) during 1970–1980 to 2.55 (10.9) during 2011–2017. Interested readers are referred to the reference [25].

### Table 2. Decadal variation of statistical characteristics of the global isothermal layer depth \((h)\) in comparison to climatology.

| Year      | Mean (m) | Standard Deviation (m) | Skewness | Kurtosis |
|-----------|----------|------------------------|----------|----------|
| 1970–1980 | 38.8     | 41.7                   | 3.97     | 27.3     |
| 1981–1990 | 55.0     | 54.6                   | 3.22     | 21.0     |
| 1991–2000 | 62.8     | 58.0                   | 2.95     | 18.4     |
| 2001–2010 | 66.3     | 61.5                   | 2.82     | 17.0     |
| 2011–2017 | 67.5     | 61.7                   | 2.70     | 15.1     |

### Table 3. Decadal variation of statistical characteristics of the global thermocline gradient \((G)\) in comparison to climatology.

| Year      | Mean \(^\circ\text{C/m}\) | Standard Deviation \(^\circ\text{C/m}\) | Skewness | Kurtosis |
|-----------|-----------------------------|---------------------------------------|----------|----------|
| 1970–1980 | 0.204                       | 0.167                                 | 1.35     | 5.02     |
| 1981–1990 | 0.162                       | 0.150                                 | 1.77     | 6.61     |
| 1991–2000 | 0.130                       | 0.133                                 | 2.29     | 9.47     |
| 2001–2010 | 0.124                       | 0.132                                 | 2.35     | 9.69     |
| 2011–2017 | 0.121                       | 0.134                                 | 2.55     | 10.90    |

### 3. Methods

#### 3.1. Describing Mixed Layer Dynamics

The connection between \( G \) (unit: \(^\circ\text{C} \text{m}^{-1}\)) and the ITL heat content \( H_{\text{ITL}} \) (unit: J m\(^{-2}\)) can be found using the conservation of heat in the ITL [1,3–5,26]

\[
\frac{\partial H_{\text{ITL}}}{\partial t} = \rho_0 c_p h T_I - \mathbf{v} \cdot \nabla T_I - \frac{Q}{\rho_0 c_p h} \Lambda \frac{w_e h}{T} \Delta T, \Delta T \equiv T_I(t, r) - T_{th}(t, r) \tag{1}
\]

where \( \mathbf{v} \) (unit: m s\(^{-1}\)) is the bulk ITL horizontal velocity vector; \( h \) is the isothermal layer depth (unit: m); \( T_I \) is the ITL temperature (unit: \(^\circ\text{C}\)); \( Q \) (unit: W m\(^{-2}\)) is the net heat flux at the ocean surface (upward positive); \( w_e \) (unit: m s\(^{-1}\)) is the entrainment velocity; \( \Lambda \) is the step function taking 0 if \( w_e < 0 \), and 1
otherwise due to the second law of the thermodynamics; $\Delta T$ is the temperature difference between ITL and thermocline; $T_h(t, r)$ is the thermocline temperature (unit: °C). It is reasonable to assume that the temperature difference is proportional to the thermocline gradient, $\Delta T = \gamma G$, with the proportionality $\gamma$ (unit: m). Using conservation of mass in the ITL gives the $H_{ITL}$ equation

$$\frac{\partial H_{ITL}}{\partial t} = -\mathbf{v} \cdot \nabla H_{ITL} - \rho_0 c_p h_0 \mathbf{v} \cdot \nabla T_h - \rho_0 c_p (T_h - T_i) \hat{w}_{2h} - Q - \hat{\Lambda} \rho_0 c_p \hat{w} \left[ \gamma G - (T_i - T_h) \right]$$

(2)

where $\hat{T}_i$ is the temperature below the ITL; the last term in the right-hand side of (2) occurs only the mixed layer dynamics and thermodynamics are included. For the entrainment regime ($w_e > 0, \hat{\Lambda} = 1$), the thermocline gradient $G$ is related negatively to $\partial H_{ITL}/\partial t$. Strong (weak) thermocline gradient causes the decrease (increase) in $H_{ITL}$. Such an entrainment effect does not show up with the upper ocean heat content with fixed depth ranges commonly used in oceanography such as 0–300 m, 0–400 m, 0–700 m, 0–750 m, and 0–2000 m.

### 3.2. Methodological Procedure

For each observational CTD/XBT temperature profile $T(t, r, z)$ from the first dataset WOD18 [22], a pair of $[G(t, r), h(t, r)]$ is identified from the third dataset with the same time $t$ and horizontal location $r$. We use the 3D linear interpolation to calculate a climatological profile $T_c(r, z)$ at the observational location $(r, z)$ from four neighboring grid points of the temperature field $T_c(r_c, r_r, z_c)$ from the second dataset WOA18 [23] for the same month.

The ITL depth $(h)$ was determined from an individual temperature profile using the optimal fitting and exponential leap-forward gradient scheme (Figure 1). It contains four steps: (1) estimating the ITL gradient (near-zero), (2) identifying the thermocline gradient $G$, (3) computing the vertical gradient at each depth (non-dimensionalized by $G$), and (4) determining $h$ with a given threshold (or user input) to separate the near-zero gradient layer (i.e., the ITL) and the non-zero gradient layer (i.e., the thermocline). Figure 1 illustrates the procedures of this method. Interested readers are referred to [22–24] for detailed information.

For an observational temperature profile $T(t, r, z)$ the corresponding climatological monthly mean profile $\hat{T}(r, z)$ is obtained. With $h(t, r)$, we calculate the difference $[T(t, r, z) - \hat{T}(r, z)]$ first and then the ITL heat content ($H_{ITL}$) with the mean monthly variation removed (i.e., relative ITL heat content),

$$H_{ITL}(t, r) = c_p \rho_0 \int_{-h(t, r)}^{0} [T(t, r, z) - \hat{T}(r, z)] dz$$

(3)

where $c_p = 3985$ J kg$^{-1}$ °C$^{-1}$ is the specific heat for sea water; $\rho_0 = 1025$ kg m$^{-3}$ is the upper ocean characteristic density. Let

$$T_i(t, r) \equiv \frac{1}{h} \int_{-h(t, r)}^{0} T(t, r, z) dz, \hat{T}_i(r) \equiv \frac{1}{h} \int_{-h(t, r)}^{0} \hat{T}(r, z) dz$$

(4)

be the in-situ and corresponding climatological monthly ITL temperature. With (3) and (4), we have

$$H_{ITL}(t, r) = \rho_0 c_p h(t, r) \left[ T_i(t, r) - \hat{T}_i(r) \right]$$

(5)

After quality control, we have 1,111,647 data pairs of $[H_{ITL}(t, r), G(t, r)]$ for the global oceans from 1 January 1970 to 31 December 2017. Such a procedure to get the data pairs of $[H_{ITL}(t, r), G(t, r)]$ is depicted in the flow chart (Figure 2).
Figure 1. Determination of isothermal layer (ITL) depth ($h$) from an individual temperature profile. The 10% (70%) line represents the 10% (70%) temperature difference between the isothermal layer and deep layer.

Figure 2. Flow chart for establishing 1,111,647 data pairs of $[H_{ITL}(t, r), G(t, r)]$ for the global oceans from 1 January 1970 to 31 December 2017.

3.3. Time Series of ($H_{ITL}, G$) for Global and Regional Oceans

To further explore the temporal variability for global and regional oceans, we represent 1,111,647 ($H_{ITL}, G$) pairs into the format of $[H_{ITL}(m, \tau_i, r_j), G(m, \tau_i, r_j)]$ with $m = 1, 2, \ldots, 12$ the time sequence in months; and $\tau_i = 1970, 1971, \ldots, 2017$ the time sequence in years with $i = 1, 2, \ldots, N \ (N = 48)$, then we divide the world oceans excluding the Arctic Ocean into 12 regions (see the first column in Table 4), and average the synoptic data pairs ($H_{ITL}, G$) within each region and the year to obtain 13 time-series of $[<H_{ITL}(\tau_i)>, <G(\tau_i)>]$, including global ocean, with the time increment of a year. Differences among the 13 time-series shows the spatial variability of the yearly variation.

The trends of the time series are determined using linear regression (taking $<G(\tau_i)>$ for illustration),

$$<\dot{G}(\tau_i)> = a + b\tau, \quad b = \frac{\partial <\dot{G}(\tau_i)>}{\partial \tau} \quad (6)$$
The trend $b$ is calculated from the data $<G(t_i)>$,

$$b = \frac{S_{Gt}}{S_{\tau\tau}} = \sum_{i=1}^{N} \frac{(t_i - \tau)^2}{S_{\tau\tau}} = \sum_{i=1}^{N} \frac{(G_i - \langle G \rangle)^2}{S_{\tau\tau}} = \sum_{i=1}^{N} \frac{(G_i - \langle G \rangle)(t_i - \tau)}{S_{\tau\tau}}$$

(7)

where

$$N = 48, \langle G_i \rangle = \langle G(t_i) \rangle, \langle \tau \rangle = \frac{1}{N} \sum_{i=1}^{N} \tau_i, \langle G \rangle = \frac{1}{N} \sum_{i=1}^{N} G_i$$

(8)

The error in determining the trend $b$ is estimated by the $t$-test. For a given significance level $\alpha$, the confidence interval for the real trend $\hat{b}$ is given by

$$b - t_{\alpha/2} \frac{S}{\sqrt{S_{\tau\tau}}} < \hat{b} < b + t_{\alpha/2} \frac{S}{\sqrt{S_{\tau\tau}}}$$

$$S^2 = \frac{S_{GG} - bS_{G\tau}}{N-2}$$

(9)

where $t_{\alpha/2}$ is a value of the $t$ distribution with $(N - 2)$ degrees of freedom.

| Ocean                  | Number of Data | $\partial H_{ITL}/\partial \tau$ (W/m²) | $\partial G/\partial \tau$ (10⁻³ °C/m × yr⁻¹) |
|------------------------|----------------|----------------------------------------|-----------------------------------------------|
| Global Oceans          | 1,111,647      | 0.142 ± 0.014                          | −2.11 ± 0.31                                  |
| North Atlantic (10° N–60° N) | 335,747    | 0.128 ± 0.022                          | −1.49 ± 0.046                                 |
| Equatorial Atlantic (10° S–10° N) | 42,599    | 0.154 ± 0.036                          | −2.28 ± 0.58                                 |
| South Atlantic (10° S–60° S)   | 57,540          | 0.0824 ± 0.04                          | −2.43 ± 0.73                                 |
| Indian Ocean            | 150,789        | 0.160 ± 0.028                          | −2.77 ± 0.49                                 |
| Equatorial Pacific (10° S–10° N) | 89,924    | 0.156 ± 0.066                          | −3.51 ± 0.63                                 |
| Southern Ocean (South of 60° S) | 7942         | −0.0272 ± 0.027                        | −1.19 ± 1.6                                  |
| Western North Pacific   |                |                                        |                                               |
| (10° N–60° N, 120° E–160° E) | 101,447     | 0.139 ± 0.04                           | −2.07 ± 0.55                                 |
| Central North Pacific   |                |                                        |                                               |
| (10° N–60° N, 160° E–140° W) | 88,967       | 0.135 ± 0.028                          | −1.65 ± 0.44                                 |
| Eastern North Pacific   |                |                                        |                                               |
| (10° N–60° N, 140° W–85° W) | 91,572       | 0.104 ± 0.062                          | −2.05 ± 0.43                                 |
| Western South Pacific   |                |                                        |                                               |
| (10° S–60° S, 145° E–170° W) | 79,472       | 0.140 ± 0.037                          | −0.821 ± 0.19                                |
| Central South Pacific   |                |                                        |                                               |
| (10° S–60° S, 170° W–120° W) | 23,632       | 0.125 ± 0.045                          | −0.378 ± 0.3                                 |
| Eastern South Pacific   |                |                                        |                                               |
| (10° S–60° S, 120° W–70° W) | 16,965       | 0.005 ± 0.084                          | −1.61 ± 1.10                                 |

4. Results and Discussions

4.1. Decadal Variability of Global ($H_{ITL}$, $G$)

In analyzing global spatial and temporal variability, we divided the 1,111,647 synoptic data pairs of [$H_{ITL}(t, r), G(t, r)$] into six temporal periods: 1971–1980, 1981–1990, 1991–2000, 2001–2010, 2011–2017. For each time-period, we average the ($H_{ITL}, G$) data in 4° (longitude) × 2° (latitude) cell if the number of data pairs is larger than 5, and identify the cell with no data if the number of data pairs is less than 5. Figure 3 shows decadal variations of the global distributions of ($H_{ITL}, G$). The number of data points are on the right panels. The white grid cells denote no data or a number of data pairs less than
5. The most striking features are thermocline weakening and ITL warming. A strong thermocline gradient \((G > 0.3\, ^\circ C/m)\) occupied a vast area of the middle to high latitudes (north of 30° N) of the Northern Hemisphere as well as the eastern equatorial Pacific and Atlantic Oceans during 1971–1980, and 1981–1990. Such strong thermocline areas shrunk during 1991–2000, and almost disappeared in 2011–2017. However, \(H_{ITL}\) increased steadily from 1971–1980 to 2011–2017. There was no area with \(H_{ITL}\) of more than \(2.5 \times 10^8 \text{ J/m}^2\) in the middle to high latitudes of the Northern Hemisphere during 1971–1980. Warm areas \((H_{ITL} > 2.5 \times 10^8 \text{ J/m}^2)\) showed up in these latitudes especially the western North Atlantic Ocean and equatorial Pacific and Atlantic Oceans in 1981–1990. The warm areas increased in 1991–2000, 2001–2010, and 2011–2017.

Figure 3. Decadal distributions of synoptic relative ITL heat content \((H_{ITL}\), left panels) and thermocline gradient \((G\), right panels) of the world oceans. The white grid cells denote no data.
4.2. Trends of \(H_{\text{ITL}}, G\) for Global and Regional Oceans

The 13 time series pairs \(<H_{\text{ITL}}(\tau_i)>\), \(<G(\tau_i)>\) show the overall temporal (yearly) variability for the global and individual regional ocean. The significant level to estimate the trend of the time series is set as \(\alpha = 0.05\). The trends of \(G\) are all negative (i.e., \(\partial G/\partial \tau < 0\)) in the global ocean \((-2.11 \pm 0.31) \times 10^{-3} \, \text{C/(m \times yr)}\) (Figure 4) as well as in all the 12 regions (Figures 5 and 6). For regional oceans, the maximum weakening rate is \([-3.51 \pm 0.63) \times 10^{-3} \, \text{C/(m \times yr)}\], occurring in the equatorial Pacific \((10^\circ \text{S}–10^\circ \text{N})\). The minimum weakening rate is \([-0.378 \pm 0.3) \times 10^{-3} \, \text{C/(m \times yr)}\], appearing in the central South Pacific \((10^\circ \text{S}–60^\circ \text{S}, 170^\circ \text{W}–120^\circ \text{W})\). The trends of \(H_{\text{ITL}}\) are positive (i.e., \(\partial H_{\text{ITL}}/\partial \tau > 0\)) in the global ocean \([0.142 \pm 0.014 \, \text{W/m}^2]\) (Figure 4) as well as in the 12 regions (Figures 5 and 6) except the Southern Ocean. The maximum warm rate is \((0.160 \pm 0.028 \, \text{W/m}^2)\), occurring in the Indian Ocean. The warm rate in the Equatorial Pacific \((10^\circ \text{S}–10^\circ \text{N})\) is also high \((0.156 \pm 0.066 \, \text{W/m}^2)\).

![Figure 4. Yearly evolutions (1970–2017) of total number of observations (upper panel), relative heat content (unit: \(10^8 \, \text{J/m}^2\)) (middle panel), and thermocline gradient (unit: \(\text{°C/m}\)) (lower panel) for the world oceans excluding the Arctic Ocean. Note that the positive real number in the parentheses mean the half size of the confidence interval with the confidence level \(\alpha = 0.05\).](image)
The robust weakening trend of the thermocline gradient \( \frac{\partial G}{\partial \tau} < 0 \) and the warming trend of the isothermal layer \( \frac{\partial H_{ITL}}{\partial \tau} > 0 \) are found in global and regional oceans except the Southern Ocean, where slightly decreasing in the relative heat content \(-0.0272 \text{ W m}^{-2}\). The data are very sparse in the Southern Ocean with a total number of observations of 7942 (Figures 3 and 5f, and Table 4) and make the trends in the Southern Ocean not robust. The highest warming rate \(0.160 \pm 0.028 \text{ W m}^{-2}\) of \(H_{ITL}\) in the Indian Ocean (Table 4) is coherent with the recent results on the fastest rate of warming in the tropical Indian Ocean among tropical oceans [27].

Figure 4. Yearly evolutions (1970–2017) of total number of observations (upper panel), relative heat content (unit: \(10^8 \text{ J/m}^2\)) (middle panel), and thermocline gradient (unit: \(° \text{C/m}\)) (lower panel) for the world oceans excluding the Arctic Ocean. Note that the positive real number in the parentheses mean the half size of the confidence interval with the confidence level \(\alpha = 0.05\).

Figure 5. Same as Figure 4 except for the (a) North Atlantic Ocean (10° N–60° N), (b) equatorial Atlantic Ocean (10° S–10° N), (c) South Atlantic (10° S–60° S), (d) Indian Ocean (north of 60° S), (e) Equatorial Pacific (10° S–10° N), and (f) Southern Ocean (south of 60° S).
4.3. Comparison in the OHC Calculation between the Isothermal Layer and Fixed-Depth Layer

The dynamical characteristics are different between the isothermal layer and fixed-depth layer (Figure 7). In the isothermal layer, the vertical velocity does not cause the temperature advection since the vertical temperature gradient is near zero. The turbulent heat flux at the base of the mixed layer \( z = -h \) is downward or zero [3–5]. However, such simple dynamic features do not exist in the fixed-depth layer (0–100 m, 0–300 m, or 0–700 m), where the vertical temperature advection is not zero. The heat flux at the base of the fixed-depth layer can be either downward or upward. This causes the OHC computed for an individual water column represented by the corresponding temperature profile having the simple mixed layer dynamics (no vertical advection and downward or zero heat flux at \( z = -h \)) with the isothermal layer (i.e., HITL) and more complicated dynamics.
flux at \( z = -h \) with the isothermal layer (i.e., \( H_{\text{ITL}} \)) and more complicated dynamics (nonzero vertical advection and either downward or upward heat flux) with the fixed-depth layer (\( H_{\text{FD}, D = 100 \text{ m}}, 300 \text{ m}, 700 \text{ m}, 2000 \text{ m} \ldots \)). This makes mean value or trend of \( H_{\text{ITL}} \) more representative statistically than \( H_{\text{FD}} \). The basic dynamic characteristics of the fixed-depth layer also cause diversification in the warm trends of the OHC anomaly (see Table 1).

![Diagram of Isothermal Layer and Fixed Depth Layer](image)

**Figure 7.** Comparison between ocean heat content (OHC) for the isothermal layer and fixed-depth layer.

### 4.4. Effective Warming with the Isothermal Layer

Table 3 shows that the global isothermal layer depth has the decadal mean and standard deviation from (38.8 m, 41.7 m) during 1970–1980 to (67.5 m, 61.7 m) during 2011–2017. It is comparable with the depth range of 0–100 m. However, the warming rate of \( H_{0-100 \text{ m}} \) (0.10 W m\(^{-2}\)) during 1967–2011 (Table 1) is slightly smaller than the warming rate of \( H_{\text{ITL}} \) (0.142 ± 0.014 W m\(^{-2}\)) during 1970–2017 and even smaller for other time periods including a cooling rate of –0.04 Wm\(^{-2}\) during 2004–2011. The warming rate of \( H_{\text{ITL}} \) (0.142 ± 0.014 W m\(^{-2}\)) during 1970–2017 is comparable to the various warming rates of \( H_{0-300 \text{ m}} \) such as 0.25 W m\(^{-2}\) during 1983–2011, 0.19 W m\(^{-2}\) during 1967–2011, 0.14 W m\(^{-2}\) during 2004–2011 [11], and 0.26 ± 0.02 W m\(^{-2}\) during 1975–2009 [14]. The warming rate increases with depth for the fixed-depth layer [11]. The isothermal layer is more effective for the warming than the fixed-depth layer since \( H_{\text{ITL}} \) is comparable to \( H_{0-300 \text{ m}} \) but with the isothermal layer depth much smaller than 300 m.

### 5. Conclusions

World ocean thermocline weakening with the rate of \((-2.11 ± 0.31) \times 10^{-3} \text{ °C m}^{-1} \text{ yr}^{-1}\), along with ITL warming with the rate of \((0.142 ± 0.014) \text{ W m}^{-2}\), were identified from the three open datasets NOAA/NCEI WOD18, WOA18, and the global ocean thermocline gradient, ITL depth, and other upper ocean parameters calculated from WOD CTD and XBT temperature profiles from 1 January 1970 to 31 December 2017 (NCEI Accession 0173210) using the new definition of the upper ocean heat content (i.e., ITL heat content \( H_{\text{ITL}} \)). Such two trends occur in the global as well as regional oceans except the Southern Ocean, where slightly decreasing in the \( H_{\text{ITL}} \) was identified. Weakening thermocline reduces the resistance to the ITL deepening that causes a thick ITL with more heat stored in the ITL (ITL warming). Thermocline weakening may play roles in global climate change in addition to the greenhouse effect from the atmosphere and in phytoplankton growth because strong thermocline inhibits the nutrient pumping. Besides, the global sea surface temperature is directly related to the ITL heat content through the ocean mixed layer dynamics. It is more reasonable to use ITL heat content than the heat content with fix-depth range in climate change studies.
Author Contributions: P.C.C. developed the method, designed the project, conducted the data quality control, and wrote the manuscript. C.F. developed the code for computation and visualization. Both authors have read and agreed to the published version of the manuscript.

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Conflicts of Interest: The authors declare no conflict of interest.

Data Availability Statement: The three datasets were all downloaded at the NOAA/NCEI website with the synoptic temperature profiles from URL (https://data.nodc.noaa.gov/cgi-bin/iso?id=gov.noaa.nodc:0173210) from URL (https://data.nodc.noaa.gov/cgi-bin/iso?id=gov.noaa.nodc:0173210).

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