A Study of the Orion Cometary Cloud L1616 *

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Abstract

With its cometary appearance and a reflection nebula near its edge facing some bright Orion stars, the Lynd's cloud L1616 shows ample evidence for being affected by one or more of these massive stars. To estimate its mass and star formation efficiency as well as to determine if it is gravitationally bound, we mapped this cloud in J=1→0 transitions of $^{12}$CO and $^{13}$CO. It is found that the distribution of the emission in the line wings show clear evidence for substantial mass motions. Also, the “virial” mass of the cloud is found to be five times the actual cloud mass determined from the $^{13}$CO column density map. It is argued that this cloud has abnormally high star formation efficiency and is possibly disintegrating. The morphology and the location of the cloud indicate that it is being affected by the star $\epsilon$ Orionis which is also possibly responsible for the cloud’s unusual star formation efficiency. Over a range of values of the relevant parameters, the star is found to quantitatively satisfy the requirements of being the cause of the observed characteristics of the cloud.

Keywords: stars: formation; ISM: clouds; ISM: individual: L1616; reflection nebulae.

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1 Introduction

Massive stars affect the structure and the evolution of the clouds around them substantially. Globules and clouds with bright rims and cometary appearance are found in the vicinity of many nearby OB associations e.g. Vela (Gum nebula; Sridharan 1992), Orion (Bally et al. 1991), Cepheus (Indrani & Sridharan 1994) and Rosette (Patel, Xie & Goldsmith 1993). In addition to affecting the morphology, these stars also accelerate the globules and possibly induce star formation in them as well. There are many clouds in the Orion complex which show evidence of being affected by the nearby stars. Lynd’s dark cloud L1616 with its cometary appearance is one among them. It also harbors a bright reflection nebula NGC 1788, also known as CED 040, excited by a poor star cluster.

Study of a cloud with an associated reflection nebula offers many advantages. Since reflection nebulae mark close spatial association of relatively dense interstellar clouds with luminous stars of spectral type B1 or later, the distance to the star and hence to the cloud can be estimated to a reasonable accuracy. This allows one to determine sizes, masses and luminosities reliably. A reflection nebula with newly born stars provides an opportunity to study the effects of recent formation of stars with intermediate masses. In particular, one that harbors a new-born cluster is most suited to study cloud fragmentation. Stars, newly formed or otherwise, have significant effects on the thermal balance of a cloud. Hence, study of such a cloud where there is an identifiable dominant energy source (but not as disruptive as O stars) permits one to investigate the heating and cooling in them.

L1616 appears to be unique among the reflection nebulae. As shown in the next section, L1616 has an estimated star formation efficiency of \( \sim 14\% \), much larger than other clouds with associated reflection nebulae. The cometary appearance of the cloud, the peculiar location of the nebula near its edge facing the bright Orion belt stars, and its suspected high star formation efficiency indicate that the cluster formation in the cloud is possibly induced. Furthermore, no IRAS source with a spectrum typical of young stellar objects is found within the cloud boundary. This may suggest that the formation of the cluster has pre-empted any further star formation - a self regulatory process often invoked in the literature. Thus, L1616 seems to be an object of considerable interest. We mapped this cloud in J = 1 \( \rightarrow \) 0 transitions of both \(^{12}\)CO and \(^{13}\)CO with a view to determine its mass more reliably and to discern any mass motions that may be present. In this paper we present the maps and argue that induced star formation is most likely to be the case and that the cloud is fragmenting.

In the following section we estimate the star formation efficiencies (SFE) of a few clouds with associated reflection nebulae and show that L1616 is unique among them. In Section 3 we present the details of the observations and the maps of L1616. The results are discussed in Section 4.

2 SFE of clouds with reflection nebulae

Star formation efficiency (SFE) usually refers to the ratio of the total mass in the stars to the sum of this stellar mass and the mass of the cloud or cloud segment they are born in. We estimate the masses in these two components for the bright reflection nebulae in the following way using their optical and infrared data from the literature.

Masses of the clouds : The cloud mass can be expressed as \( 2 \times N(H_2) m(H) \Omega_c d^2 \), where \( N(H_2) \) is the molecular hydrogen column density, \( m(H) \) the atomic mass of hydrogen, \( \Omega_c \) the solid angle of the cloud and \( d \) its distance from the Sun. To estimate \( \Omega_c \) and \( N(H_2) \) reliably, the clouds need to be mapped both in \(^{12}\)CO and \(^{13}\)CO. However, for most of the reflection nebulae such maps are not available. Hence, we use their optical obscuration solid angles listed in the catalogues of dark clouds (Lynds 1962; Feitzinger & Stuwe 1984; Hartley et al. 1986). We wish to note
that only the mass in dense portions of the cloud, which the optical obscuration would trace well, may be relevant for the estimation of SFE. Molecular hydrogen column density seems to be nearly constant in clouds over a wide range of sizes (Larson 1981) and we take this to be $\sim 5 \times 10^{21} \text{ cm}^{-2}$, typical of the small molecular clouds. The masses estimated in this way will be very approximate. Nevertheless, we believe that this will not be a severe handicap for the relative comparison of SFE attempted here.

**Masses in stars:** Many optically bright reflection nebulae are also bright in far infrared (FIR) and have been detected by IRAS. Their FIR emission results from reprocessing of the radiation from the exciting stars by the dust in the surrounding cloud. In most cases, the spectral type of the brightest member of the exciting stars is also known. Then, if one assumes all stars to be of the same spectral type, a lower limit to the mass in stars is given by $4 \pi d^2 S_{\text{FIR}} M (\eta L)^{-1}$. Here $M$ and $L$, respectively, are the mass and luminosity of the brightest star in the cluster derived from its spectral type (Allen 1976), $\eta$ is the fraction of the stellar radiation that is reprocessed which is taken to be 0.3 (albedo = 0.7, Witt & Schild 1986) and $S_{\text{FIR}}$ is the FIR flux density derived in the following way using the measured flux densities in the four IRAS bands (Margulis, Lada & Young 1989):

$$S_{\text{FIR}} = \int S_\nu \, d\nu$$

$$= 2.37 \times 10^{-10} \left( S_{12} + 0.567 S_{25} + 0.154 S_{60} + 0.059 S_{100} + \frac{7.39 S_{\text{max}}}{\lambda_{\text{max}}} \right) \text{ergs}^{-1} \text{cm}^{-2}$$

In this expression the flux densities are in Jy and $\lambda_{\text{max}}$, the longest wavelength at which the flux density is measured is in $\mu$m, and $S_{\lambda_{\text{max}}}$ the corresponding flux density. The last term is the estimated flux emitted longward of $\lambda_{\text{max}}$ (Myers et al. 1987). This is obtained by assuming that $S_{\lambda_{\text{max}}}$ is also the maximum over the entire spectrum, and that the spectrum is like that of a blackbody for wavelengths longer than $\lambda_{\text{max}}$. However, it should be noted that if star formation is very recent, as the luminosities of protostars change considerably with time (Lada 1991), the above estimate of mass in stars can be inaccurate.

Since the masses of both the components depend similarly on the distance, their ratio is independent of it resulting in the following expression for the minimum SFE.

$$SFE (\%) = \frac{100}{1 + X}$$

where,

$$X = \frac{M_\ast}{M_C} = \frac{\int S_{\text{FIR}} M}{\eta L} \times \frac{1}{(2 m_H N_{\text{H}_2} \Omega_C)} = \frac{1.286 \times 10^9 \left( M/M_\odot \right) \left( S_{\text{FIR}}/\text{erg s}^{-1} \text{ cm}^{-2} \right)}{(L/L_\odot) \left( \Omega_C/\mu \text{ steradian} \right)}$$

Thus, the only quantities entering the estimates are: the solid angle of the clouds, the IRAS flux densities of the associated nebulae and the mass and the luminosity of the exciting star with the earliest spectral type. We use this approach to determine SFE of a few clouds with associated reflection nebulae. In Table 1 we have listed the names of the nebulae (row 1), of the brightest stars exciting them (row 2), their spectral type (row 3), mass (row 4) and luminosity (row 5), the names of the associated clouds (row 6), their solid angle (row 7) and mass (row 8), names of the associated extended IRAS
sources (row 9), their flux densities in the four bands (row 10-13), the FIR fluxes $S_{FIR}$ (row 14), and their estimated SFE (row 15). The spectral type of the stars exciting the nebulae have been taken from the catalogues of reflection nebulae (van den Bergh 1966; van den Bergh & Herbst 1975). Table 1 shows that L1616 has the highest estimated SFE. Two other clouds, L1630 and SC064, also have high estimated SFE but their masses are likely to be under-estimates owing to their large physical sizes. This can be seen from the following. One could take the volume density of molecular hydrogen, $n_{H_2}$, in the clouds to be the same instead of the column density. Then, for spherical clouds, the new SFE$_V$ is given by,

$$SFE_V (%) = 100 \left( \frac{X_V}{1 + X_V} \right)$$

where,

$$X_V = 1470 \times \frac{X}{(d/pc) (\sqrt{\Omega_C/\mu \text{ steradian})}}$$

A value of 1100 cm$^{-3}$ has been assumed for $n_{H_2}$ such that SFE and SFE$_V$ are the same for the cloud L1616 (This choice does not affect the relative values of SFE$_V$ derived). Row 16 in Table 1 lists SFE$_V$ calculated this way using distances (last row) taken from the literature (Racine 1968; Herbst 1975). Table 1 shows that SFE$_V$ for the two clouds, L1630 and SC064, are much smaller than that of L1616. Nevertheless, they also appear peculiar and merit further studies. Before leaving this section, we wish to emphasise that the SFEs calculated here are very approximate. The estimated stellar mass being a minimum makes the calculated SFE to be a lower limit. But, this is made quite uncertain because of the error in the estimate of the cloud mass. For example, the assumption that the density is the same for all the clouds may not be valid. In this sense, both the small clouds (L1616 & SG033) having high SFEs may be a bias effect resulting from them being denser. Thus, detailed CO observations are needed to confirm these SFEs. We have carried out such observations for the cloud L1616.

3 Observations

Above estimates suggest that, among the clouds with associated reflection nebulae, the cloud L1616 has an abnormally high SFE. However, as mentioned already, it is necessary to make detailed CO maps to determine the cloud mass and hence the SFE more reliably. Such maps would also help to ascertain if mass motions are present. For this purpose, we mapped the cloud L1616 in $J = 1 \rightarrow 0$ transitions of $^{12}$CO and $^{13}$CO with a $\sim 1'$ beam and a grid-point spacing of one beam. The observations were carried out during the winters of 90-91 and 91-92 using the 10.4m millimeterwave telescope at the Raman Research Institute campus, Bangalore (for a brief description of the telescope see Patel 1990; Sridharan 1993). A filter-bank spectrometer with 250 kHz (0.65 kms$^{-1}$) resolution covering a total bandwidth of 64 MHz was used. During the observations, pointing was checked by beam switched continuum scans on Jupiter (see Patel 1990 for details) and the rms pointing error was estimated to be $\sim 12''$. An ambient temperature load was used for calibration. During the observations the DSB $T_{sys}$ ranged from 600 K to 1200 K. Frequency switching by 15.25 MHz was used for all the observations and the spectra obtained were appropriately combined. Third order polynomials were fitted to estimate and remove the curved baselines. Most of the final spectra had an rms noise of $\sim$0.25 K and the estimated rms error on the velocities is $\sim 0.3$ kms$^{-1}$. We estimate the forward spillover and scattering efficiency, $\eta_{fss}$, to be 0.57 and 0.63 at the $^{12}$CO and $^{13}$CO frequencies, respectively, by comparing the measured antenna temperatures on the calibration sources (mostly Ori A) with the source brightness temperatures reported in the literature (taken to be 73 K and 16 K at the two frequencies, respectively, for Ori A). We have also corrected the spectra for the elevation dependence of $\eta_{fss}$.
The kinetic temperature and the $^{13}$CO column density were obtained from the spectra using the relations given by Dickman (1978), assuming that $^{13}$CO is optically thin, and that both $^{12}$CO and $^{13}$CO have the same excitation temperatures. These relations take into account the 2.7 K microwave background as well as the fact that the usual Rayleigh-Jeans approximation ($h\nu \ll kT$) is not valid at millimeter wavelengths for the typical kinetic temperatures that obtain in the molecular clouds. Figures 1 to 4 show the distributions of the $^{13}$CO column density, the kinetic temperature, the equivalent width and the integrated line intensity ($\int T\, dV$) in the cloud L1616. The $^{12}$CO spectra were used to obtain the last three quantities while the $^{13}$CO spectra yielded the first. The ellipse in Figs. 1 to 4 outlines the I band image of the nebula NGC 1788 (see Plate 62 of Witt & Schild 1986) associated with L1616. Its major and minor axes are \( \sim 3.4' \) and \( \sim 2.1' \) long, respectively. It is centred at the position of the IRAS source with \( RA = 5^h\, 4^m\, 25.8^s \) and \( DEC = -03^\circ\, 25'\, 5'' \) (hereafter, the centre) and oriented 45° with respect to the west. The star, HD 293815, of spectral type B9V is the brightest visible member of the cluster of stars illuminating the nebula NGC 1788. It lies \( \sim 0.8' \) away from the centre in the NW direction.

Following are the notable features in the maps:

1. The $^{13}$CO column density peaks at \( \sim 3' \) west of the centre with a shoulder around the nebula and falls off gradually and more or less symmetrically from the peak.
2. The temperature distribution is more or less centered on the nebula with its peak at 1' east of the centre and hence not coincident with the column density peak. This indicates that the radiation from the stars is the dominant energy source.
3. The spatial distribution of equivalent widths is more or less symmetrically distributed and has its peak coincident with the column density peak. Fig.3 shows that most parts of the cloud have equivalent line widths greater than \( \sim 2 \) km s\(^{-1}\).
4. The contour map of the derived integrated $^{12}$CO line intensity distribution in L1616 bears similarity to both $^{13}$CO column density (Fig.1) and kinetic temperature (Fig.2) distributions. For example, the two peaks, one each to the east and west of the centre, correspond to the temperature and column density peaks, respectively. This similarity implies that although the $^{12}$CO integrated line intensity map has column density information, it is substantially altered by the distribution of the temperature in the cloud. Hence, using integrated $^{12}$CO line intensities to trace the column density distributions of molecular hydrogen is not always reliable.

### 4 Discussion

As stated earlier, one of the primary objectives of the observations was to determine the cloud mass more reliably. The mass of the cloud estimated from the $^{13}$CO column density map presented in the previous section using a N\(_{\text{H}_2}\) to N\(_{^{13}\text{CO}}\) conversion factor of \(5 \times 10^5\) (Dickman 1978) is \(\sim 169\, M_\odot\). One can also use the integrated $^{12}$CO line intensity map to determine the cloud mass. The mass found this way using a value of \(2.3 \times 10^{20}\, \text{cm}^{-2}/\text{K km s}^{-1}\) for the I\(_{^{12}\text{CO}}/N_{\text{H}_2}\) ratio (Strong et al. 1988) is \(\sim 193\, M_\odot\). The two mass estimates are in good agreement with each other. We take their mean, which is \(\sim 180\, M_\odot\), to be the cloud mass. This agrees well with our rough estimate presented in the beginning, although larger by a factor of \(\sim 1.15\). The SFE calculated using this new and more reliably determined cloud mass is \(\sim 12\%\) (estimated total mass of the stars/stellar and cloud mass). This is still large compared to the average SFE value of \(\lesssim 3\%\) (Evans & Lada 1991) found for the nearby molecular clouds.

One can also obtain the mass from the cloud-averaged line width, provided the cloud is in virial equilibrium. For L1616, since the line is wide over most parts of the cloud, the actual cloud-averaged
line width turns out to be $\sim 2.7 \text{ km s}^{-1}$. The corresponding virial mass required to keep the cloud bound is $1000 M_\odot$, five times larger than the estimated mass. Conversely, if the cloud is bound, its detected mass of $\sim 180 M_\odot$ would imply a cloud-averaged line width of only $\sim 1.25 \text{ km s}^{-1}$. Thus, it appears that the energy input from the stars in the cluster is fragmenting the cloud. The excess turbulent motions of $\sim 1.5 \text{ km s}^{-1}$ over and above that needed for virial equilibrium and the present cloud size of $\sim 2 \text{ pc}$ suggest that the fragmentation is possibly happening for the past 1 to 2 Myr.

The spatial distributions of emission in the linewings shown in Fig.5 also indicate the disturbed state of the cloud. The average emission from the material in the velocity ranges 5.4 to 6.7 km$s^{-1}$ (thin) and 8.7 to 10.4 km$s^{-1}$ (thick), respectively, are shown superimposed one over the other. The blueshifted and redshifted emissions have large spatial extents and distinct peaks, each a little away from the centre. They clearly indicate that substantial mass motion is present, possibly caused by the activity of the stars in the cluster. For example, the spherical redshifted emission, whose peak is coincident with the column density peak, is found to contain $\sim 10\%$ of the cloud mass. The conclusion that the mass motions in the cloud is substantial is further supported by the coincidence of the column density peak with the line width peak. It is also consistent with the conclusion of de Vries et al. (1984) who, from a systematic survey of reflection nebulae, found that 60\% of the clouds with associated reflection nebulae have broad lines; the enhanced emission in the wings and local line broadening arise from mass motions due to the dynamical interaction between the molecular cloud and the stars illuminating the nebulae. Incidentally, the energy contained in the mass motions is $\sim 10^{45}$ ergs which is less than $\sim 0.1\%$ of the energy radiated by the stars in the cluster over the past few million years.

Having found that the cloud L1616 has abnormally high SFE and shows clear signs of disintegration, we set out to determine the possible cause. Its high SFE and cometary appearance suggest an external cause. Figure 6 presents a wide angle view of the portion of the sky around the cloud L1616 showing its cometary tail towards $30^\circ$ southwest and all nearby stars of spectral type earlier than B2. Only such stars can affect the morphology and kinematics of nearby clouds significantly as well as cause implosion in them. Table 2 provides the details of these stars taken from the literature (Hirshfeld & Sinnott 1985). The projected tail is directed nearly perpendicular to the galactic plane and its extension points to stars 3 and 4 as possible causes. However, when their distances from the cloud and their spectral types are considered, it is clear that star 3 ($\epsilon$ Orionis, a blue supergiant) is the most influential one. Its present surface temperature and luminosity estimated from its spectral type (B0Ia) are $\sim 28000 \text{ K}$ and $2.5 \times 10^6 L_\odot$, respectively (Allen 1976). This implies that the spectral type of its main-sequence (MS) progenitor is O6 with a mass of $\sim 35 M_\odot$ and a lifetime of $\sim 4.3$ Myr. Such a star may have accelerated the cloud through the rocket effect (Oort & Spitzer 1955), as well as causing it to implode and form the star cluster. Earlier works (e.g. Bertoldi 1989, Bertoldi & McKee 1990) have shown that a cloud can implode as well as acquire a tail structure in such a process. A simple estimate of the time taken by the cloud to cover the current star-cloud separation of 50-70 pc using the typical induced velocities of 10-15 km$s^{-1}$ (Bertoldi and McKee 1990) yields a value of $\sim 5$ Myr. This being in good agreement with the expected age of the star $\epsilon$ Orionis suggests that its progenitor could have propelled the cloud L1616 to its present position from an initial location close to the star within the stellar life-time. In the following, we proceed to check this suggestion more quantitatively.

Using two dimensionless parameters viz. the column density parameter, $log(\eta)$, and the initial shock velocity parameter, $log(\nu)$, Bertoldi (1989) has classified clouds exposed to ionising radiation. The cloud L1616, given its radius of $\sim 1$ pc and molecular hydrogen density of 1200 cm$^{-3}$, has a value of $\sim 3.24$ for $log(\eta)$. The upper and lower bounds to its initial distance of 50 pc (set by the present projected cloud separation) and 1 pc, respectively, constrain $log(\nu)$ to lie between -0.62 to 1.08. These values for the parameters place L1616 in region II of his Fig.1. In this case, almost all of the ionising radiation will be absorbed by the recombing gas streaming off the ionisation front and the ionisation front can be considered thin relative to the cloud size. In this approximation, the temporal evolution
of the parameters (mass, radius, ion density, distance and speed) of a cloud exposed to radiation from a massive star are described by the equations presented in Appendix A. There are three unknowns in the problem: the escape velocity of the ionised plasma, \( v_i \), the fractional cloud velocity at present, \( \frac{v}{v_i} \) and the ratio of the initial and the final values of the cloud distance, \( \frac{x_i}{x_f} \). However, the latter two are not independent (as can be seen from equation A4) thus reducing the independent unknowns to two. The only constraint is that the cloud moves from \( x_0 \) to \( x_1 \) within the interaction time-scale set by the age of the star. This is bound by its MS life-time of \( \sim 4.3 \) Myr and its maximum age of \( \sim 5 \) Myr.

Fig.7 shows a contour plot of the time needed to move to the present separation, taken to be 50 pc, as a function of \( x_0 \) and \( v_i \). For the same value of \( v_i \) two initial positions, one closer to the star and another closer to the cloud, result in the same time of travel. The former solution is preferred as it results in a larger average density enhancement ahead of the shock front (which goes as \( \ln(\frac{x_i}{x_0}) \)), thus increasing the chances of external triggering. Although, \( x_0 \) and \( v_i \) can not be uniquely fixed, it is clear that, for reasonable values of these parameters, the progenitor of the star \( \epsilon \) Orionis could have caused the propulsion of the cloud to its present position within the stellar life-time. For a temperature of 10000 K, the sound speed in the ionised plasma is \( \sim 11.4 \) \( \text{km s}^{-1} \) and, observationally, the plasma in a bright condensation in M16 is found to be streaming with a speed of \( \sim 13 \) \( \text{km s}^{-1} \) (Courtes, Cruvellier & Pottasch, 1962). Hence, we take \( v_i \) to be typically between 12 and 15 \( \text{km s}^{-1} \). The projected and 3-D separation between the star and the cloud are 50 pc and 70 pc, respectively. If these are taken to be the lower and upper limits to the distance travelled in the maximum available time of \( \sim 5 \) Myr, along with a corresponding escape speed for the plasma of 12 and 15 \( \text{km s}^{-1} \), the needed initial separations turn out to be 5 pc and 4 pc, respectively. Fig.8 shows the variation of the cloud parameters with time for these two cases. The corresponding initial mass, initial radius and the present speed of the cloud for the two cases are: 535 \( M_\odot \), 1.29 pc, 13.1 \( \text{km s}^{-1} \) and 595 \( M_\odot \), 1.34 pc, 18.0 \( \text{km s}^{-1} \), respectively. For the lower velocity case, the measured radial velocity of \( \sim 7.5 \) \( \text{km s}^{-1} \), which includes a galactic differential rotation contribution of \( \sim 3.7 \) \( \text{km s}^{-1} \), would imply a proper motion velocity of \( \sim 12.5 \) \( \text{km s}^{-1} \). This would require that its direction of motion makes an angle \( \sim 73^\circ \) with respect to the line of sight (LOS) or, equivalently, the difference in the distance to the star and the cloud from the Sun is not more than \( \sim 15 \) pc. This is within the errors (\( \sim 20\% \)) of the estimated distances to \( \epsilon \) Orionis and L1616 of 370 pc and 420 pc, respectively. Incidentally, the density \( \rho_2 \) behind the shock front varies from 150 to 15 \( \text{cm}^{-3} \) (see Fig.8). The density ahead of the front \( \rho_1 \) is approximately,

\[
\rho_1 = 2 \rho_2 \left( \frac{v_2}{v_i} \right)^2
\]

\[
= 4 \rho_2 \left( \frac{T_2}{T_1} \right)^2
\]

(4)

where, \( v \)'s and \( T \)'s are the corresponding sound speeds and temperatures. Taking \( T_1 \) and \( T_2 \) to be 40 K and 10000 K, respectively, \( \rho_1 \) is found to vary from \( 10^2 \) to \( 10^4 \) over the last 5 Myr. This substantial density enhancement in the frontside of the cloud over a long period could have caused it to implode and form the cluster. The cloud fragmentation timescale estimated earlier is consistent with this scenario. A quantity which could have substantiated this further is the tail-stretching timescale. However, it could not be obtained as no velocity gradient along the tail was discernible. This may be due to the insufficient velocity resolution used (0.65 \( \text{km s}^{-1} \) at 115 GHz). Also, it may be difficult to determine any possible gradient due to the confusion resulting from the mass motions in the cloud generated by the cluster. Nevertheless, assuming that the tail makes an angle of \( \sim 73^\circ \) with the LOS and the projected length of the tail is \( \sim 2.5 \) pc, the upper limit to the velocity gradient can be translated to a lower limit to the tail stretching time-scale of \( \sim 1.1 \) Myr. This agrees with the available travel time, but does not constrain it well. In conclusion, the above discussion is consistent with the hypothesis that the star \( \epsilon \) Orionis has been the external trigger. A measurement of the proper motion velocity of
HD293815, the brightest star exciting the reflection nebula, will confirm this.

5 Summary

We shall now summarise our main findings. Our main objectives were to determine the mass of the cloud L1616 and to find out if large scale mass motions are present. For this purpose, we mapped this cloud in the $J = 1 \rightarrow 0$ transitions of both $^{12}$CO and $^{13}$CO. We have presented the distributions of the $^{13}$CO column density, the kinetic temperature, the equivalent width and the integrated line intensity in the cloud. They clearly indicate that the star cluster exciting the reflection nebula is the dominant energy source and that substantial mass motions are present in the cloud. The masses determined from the maps of $^{13}$CO column density and $^{12}$CO integrated line intensity are in agreement with each other and suggest that the mass of the cloud L1616 is $\sim 180 \ M_\odot$. This confirms the high star formation efficiency suspected in this cloud if the stellar mass estimated from the FIR fluxes is reasonably correct. However, the virial mass estimated from the cloud-averaged line width of $\sim 3 \ \text{km s}^{-1}$ is $1000 \ M_\odot$. This is much larger than the above estimates and suggests that the cloud may be disintegrating. The evidence for mass motions supports this. The cometary appearance, the location of the star cluster near the edge facing the bright Orion stars, and the estimated high star formation efficiency suggest that the cluster formation may have been externally triggered. The star $\epsilon$ Orionis located opposite to the tail direction is the most likely external trigger. It is found that this star could have propelled the cloud from its initial distance to its present position in a time-scale of $\sim 5 \ \text{Myr}$ for reasonable values of the two parameters viz. the initial distance to the cloud from the star and the escape velocity of the ionised gas. If the cluster-formation is externally triggered, the average density enhancement must have been high. This requires that the cloud was initially close to the star which leads to a large space velocity of $\sim 13 \ \text{km s}^{-1}$ at present. Then, the measured radial velocity requires the cloud to have a proper motion velocity of $\sim 12 \ \text{km s}^{-1}$.

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An early type star, when first formed, is expected to pump UV photons into the surrounding ISM rather abruptly. Many dense molecular condensations within its Stromgren radius (which is 12 pc for a star of spectral type O6V for an assumed value of 10 cm$^{-3}$ for the mean hydrogen density of the surrounding medium) will experience a weak R-type ionisation front passing quickly around them, after which the stellar UV radiation will drive an ionisation front into the denser cloud. The ionised hydrogen produced on the side of the cloud facing the star, being at a higher pressure than the gas outside owing to its higher density, would expand producing a recoil on the cloud and thus accelerate it away from the star. The loss of this gas also results in the reduction of the cloud mass, and hence the cloud radius. In this appendix we derive equations describing how the cloud’s position $x$, radius $r$, mass $m$ and relative velocity with respect to the star $v$ change with time under certain assumptions.

Let $v_1$, $m_1$ and $r_1$, respectively, be the present velocity, mass and radius of the cloud and $x_0$ and $x_1$, respectively, be its initial and present distance from the star $\epsilon$ Orionis. Integrating the equation of motion, taking $v$ to be zero initially, one gets the following result for rocket acceleration,

$$M(v) = M_1 \exp\left(\frac{v_1 - v}{v_i}\right) = M_1 \exp(z_1 - z)$$ (A1)

Here, $z$ is $v$ expressed as a fraction of $v_1$, the velocity at which the ionised gas escapes. The latter is nearly equal to the sound speed in the ionised plasma which is $\sim 11.4$ kms$^{-1}$. In obtaining the above result we have ignored the deceleration due to sweeping up of matter. A cloud of radius $\sim 1$ pc ploughing through a medium with an average hydrogen density of 1 cm$^{-3}$ over a distance of $\sim 70$ pc would sweep up only a mass of $\sim 4$ M$_\odot$. Since this is much smaller compared to the present cloud mass, deceleration due to it can be ignored. This is particularly justified in the case of L1616 because the cloud is at an altitude of $\sim -190$ pc while the star $\epsilon$ Orionis is at an altitude of $\sim -120$ pc (Their galactic longitudes and latitudes are: [203.5, $-24.7$] and [205.2, $-17.2$], respectively). Thus, most of its motion would have taken place at high altitudes, nearly perpendicular to the galactic plane, where the general ISM density is likely to be quite low resulting in negligible swept-up mass.

The rate at which the cloud loses mass is given by $m_p n(z) \pi r^2(z) v_i$, where $m_p$ is the mass of a proton and $n(z)$ is the number density of hydrogen ions just behind the ionisation front (Spitzer 1978). Here, both $n$ and $r$ are taken to depend on $z$. As the cloud recedes from the star, the ionising photon density at the cloud surface will vary and hence cause $n$ to vary. Since the cloud loses mass, the cloud radius would also change. If the mean density is conserved, then $r(z)$ is given by,

$$r(z) = r_1 \exp\left(\frac{z_1 - z}{3}\right)$$ (A2)

Assuming that the gas expands spherically and that the recombinations occurring in it nearly completely shield the stellar UV photons, one obtains the following expression for $n(z)$ (Spitzer 1978),

$$n(z) = \frac{1}{x(z)} \sqrt{\frac{3 N_c}{4\pi\alpha r(x)}}$$ (A3)

where, $N_c$ is the stellar output rate of ionising photons and $\alpha$ is the effective recombination probability.
for hydrogen taken to be $2.6 \times 10^{-13}$ cm$^3$s$^{-1}$. Now, equating the mass loss rate to $\frac{M(z)}{v_i} \times \frac{dv}{dt}$ and solving for $x(z)$ using the fact that $\frac{dv}{dt} = v_i z \frac{dx}{dt}$ one obtains,

$$x(z) = x_0 \exp \left( \beta \left[ \exp(0.5z_1) - (1 + 0.5z) \exp \left( \frac{z_1 - z}{2} \right) \right] \right)$$

(A4)

where, \[ \beta = \frac{4M_1}{m_p} \sqrt{\frac{4\alpha}{3\pi N_c r_i^2}} \] (A5)

It is worth noting that, in addition to their boundary values, the cloud variables described by the above equations depend only on $z$ and not on $v$ or $v_i$ themselves. The fact that the infinitesimal time $dt$ taken for the cloud to move by an infinitesimal distance $dx$ depends on the velocity and acceleration during that period results in the following equation:

$$dt(z) = \frac{\beta x(z) \exp((z_1 - z)/2)}{8v_i} \left[ -z + \sqrt{z^2 + \frac{16 \exp((z - z_1)/2) dx}{\beta x(z)}} \right]$$

(A6)

Since it was not possible to obtain a closed form solution, we have numerically integrated this equation to get the time as a function of $z$. In the graphs shown in Fig.8, the time axis was derived in this way.
Table 1. Reflection nebulae – star formation efficiencies

| Nebula | vdB017 | vdB013 | vdB033 | vdB052 | vdB055 | vdB123 | VHE05 | VHE30 | VHE17 | VHE28 |
|--------|--------|--------|--------|--------|--------|--------|-------|-------|-------|-------|
| Star   | +30°549 | +30°540 | 293815 | 37903  | 38023  | 170634 |       |       |       |       |
| SpT    | B8V    | B8V    | B9V    | B1.5V  | B4V    | B7V    | *     | *     | B1V   | B5Vp  |
| M* (M☉) | 4.1    | 4.1    | 3.6    | 12.7   | 7.7    | 4.7    | 3.2   | 3.2   | 14.2  | 6.5   |
| L* (L☉) | 179    | 179    | 117    | 6887   | 1406   | 283    | 79    | 79    | 9727  | 794   |
| Cloud  | L1450  | L1452  | L1616  | L1630  | L1641  | L572   | SC025 | SC102 | SG033  | SC064 |
| ΩC (µstr.) | 358    | 358    | 12     | 611    | 611    | 1322   | 171   | 764   | 8     | 212   |
| M* (M☉) | 6739   | 2227   | 157    | 13862  | 6617   | 18935  | 2279  | 52259 | 547   | 3991  |
| IRAS   | X0326  | X0322  | X0504  | X0539  | X0539  | X1827  | X0809 | X0916 | X0833  | X0857 |
| name   | +312   | +307   | -034   | -019   | -081   | +012   | -356  | -482  | -405  | -435  |
| 12µm (Jy) | 91     | 6      | 30     | 2090   | 52     | 32     | 3     | 14    | 117   | 984   |
| 25µm (Jy) | 30     | 6      | 68     | 177700 | 53     | 65     | 4     | 28    | 190   | 4410  |
| 60µm (Jy) | 1080   | 20     | 323    | 93400  | 304    | 375    | 14.5  | 196   | 1100  | 26400 |
| 100µm (Jy) | 1190   | 49     | 594    | 77400  | 787    | 750    | 29    | 392   | 2700  | 24300 |
| S_FIR (10^{-10}) | 1024   | 45     | 467    | 302246 | 553    | 536    | 27    | 266   | 1784  | 25530 |
| SFE (%) | 0.84   | 0.04   | 13.42  | 10.55  | 0.06   | 0.09   | 0.08  | 0.18  | 4.04  | 11.32 |
| SFE (%) | 0.13   | 0.01   | 13.42  | 1.23   | 0.01   | 0.01   | 0.01  | 2.20  | 2.47  |       |
| Dist. (pc) | 501   | 288    | 417    | 550    | 380    | 437    | 1318  | 955   | 955   | 501   |

A (*) mark in SpT row indicates that the earliest stellar spectral type is not known and has been assumed to be A0V. In cloud name prefix L stands for Lynd’s cloud, SC for southern dark cloud and SG for southern dark globule.

Table 2. Luminous stars near the cloud L1616

| Index | SAO no. | Dist. (pc) | SpT | α_1950 | δ_1950 |
|-------|---------|------------|-----|--------|--------|
| no.   | no.     |            |     | h m s   | ° ' ″  |
| 1     | 132406  | 500        | O9.5V | 5 36 14 | -2 37 39 |
| 2     | 132387  | 540        | B1.5V | 5 35 25 | -4 50 32 |
| 3     | 132346  | 370        | B0Ia | 5 33 41 | -1 13 56 |
| 4     | 132269  | 560        | B2V  | 5 31 31 | -1 04 07 |
| 5     | 132210  | 550        | B2V  | 5 28 55 | -6 44 41 |
| 6     | 132222  | 560        | B0V  | 5 29 31 | -7 20 13 |
| 7     | 112830  | 560        | B1.5V | 5 27 19 | +1 45 05 |
| 8     | 112861  | 470        | B1.5V | 5 28 37 | +3 15 21 |
| 9     | 112734  | 490        | B1V  | 5 22 09 | +1 48 08 |
| 10    | 112697  | 470        | B1V  | 5 20 12 | +3 29 52 |
| 11    | 131451  | 460        | B2V  | 4 41 41 | -8 35 44 |

L1616: 420 Cloud 5 04 30 -3 25 00
Figure Captions

Fig.1 : Distribution of $^{13}$CO column density in L1616. The ellipse marks the position, the orientation and the extent of the I band image of NGC 1788. The peak contour level is $3.2 \times 10^{16}$ cm$^{-2}$ and the spacing is $0.2 \times 10^{16}$ cm$^{-2}$.

Fig.2 : Distribution of $^{12}$CO kinetic temperature in L1616. The elliptical outline of the I band image of NGC 1788 is shown. The peak contour level is 30 K and the spacing is 2 K.

Fig.3 : Distribution of equivalent width obtained from $^{12}$CO spectra. The innermost contour level is 3.1 kms$^{-1}$ and the spacing is 0.2 kms$^{-1}$. The outer open contours are possibly artefacts arising from the uncertainty in the measured widths owing to poorer signal to noise ratios. The portions of the cloud material lying between the open and closed contours have linewidths $> \sim 2$ kms$^{-1}$, but are not shown for the sake of clarity. The ellipse outlines the I band image of NGC 1788.

Fig.4 : Distribution of integrated $^{12}$CO line intensity in L1616. The I band image of NGC 1788 is outlined by the ellipse. The peak contour level is 33 Kkms$^{-1}$ and the spacing is 2 Kkms$^{-1}$.

Fig.5 : The thin and thick contours show the distribution of $^{12}$CO emission averaged over the velocity ranges 5.4 to 6.7 kms$^{-1}$ and 8.7 to 10.4 kms$^{-1}$, respectively. The elliptical I band image of NGC 1788 is also marked. The peak contour level is 5 K with a spacing of 1 K.

Fig.6 : Bright Orion stars near the cloud L1616. Its cometary tail is indicated. The details of the stars are given in Table 2. Star 3 is $\epsilon$ Orionis, a blue supergiant. Owing to its nearness to the cloud and earlier spectral type, progenitor of $\epsilon$ Orionis is more likely to be responsible for both the morphology and the efficient star formation of the cloud L1616.

Fig.7 : Shows the contour plot of the time taken by the cloud L1616 to travel from its initial position to its present one, taken to be 50 pc, as a function of the initial distance, $x_0$, and the escape velocity of the ionised gas, $v_i$, when accelerated by the star $\epsilon$ Orionis through the rocket effect. Contours are labelled with the time taken in units of million years. The parameter space between the 4.2 Myr and 5.1 Myr contours is favourable for the star being the external trigger.

Fig.8 : Shows the time evolution of the cloud parameters as it gets accelerated through the rocket effect. In each of the graphs, thin and thick curves correspond to two cases with $v_i$, $x_0$ and $x_1$ of 12 (15) kms$^{-1}$, 5 (4) pc and 50 (70) pc, respectively. Distance from the star, ion density just behind the shock front, velocity and mass expressed as a fraction of its present value, 180 M$_{\odot}$, are the respective parameters plotted in the four graphs.
