De novo design of a non-local β-sheet protein with high stability and accuracy

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β-sheet proteins carry out critical functions in biology, and hence are attractive scaffolds for computational protein design. Despite this potential, de novo design of all-β-sheet proteins from first principles lags far behind the design of all-α or mixed-α/β domains owing to their non-local nature and the tendency of exposed β-strand edges to aggregate. Through study of loops connecting unpaired β-strands (β-arches), we have identified a series of structural relationships between loop geometry, side chain directionality and β-strand length that arise from hydrogen bonding and packing constraints on regular β-sheet structures. We use these rules to de novo design jellyroll structures with double-stranded β-helices formed by eight antiparallel β-strands. The nuclear magnetic resonance structure of a hyperthermostable design closely matched the computational model, demonstrating accurate control over the β-sheet structure and loop geometry. Our results open the door to the design of a broad range of non-local β-sheet protein structures.
β-hairpins\(^1\), there was no correlation between β-arch loop length and side chain pattern. Instead, each loop ABEGO type, because of the way in which it twists and bends the polypeptide chain\(^1\), is associated with a specific flanking residue side chain pattern (Fig. 1b).

The next level of non-local interaction complexity in all-β folds involves strand pairing (parallel or antiparallel) between two β-arches forming a β-arcade (Fig. 1d), a common structural motif in naturally occurring β-solenoids\(^1\)\(^2\). Because the β-arch loops are stacked in register, the side chains adjacent to one β-arch loop are likely to have the same orientation as the side chains adjacent to the second β-arch loop; analysis of naturally occurring β-arches confirms that the side chain patterns of the two β-arch loops are indeed correlated (Fig. 1d, middle).

**Jellyroll design principles.** The double-stranded β-helix can be regarded as a long β-hairpin wrapped around an axis perpendicular to the direction of β-strands, with β-helical turns formed by the pairing between β-arcades (Fig. 2a). In the compact folded structure, two antiparallel β-sheets pack against each other in a sandwich-like arrangement, with the first strand paired to the last, and all β-strands are connected through β-arch loops except for the central β-hairpin. We aimed to design β-helices with three β-arcades forming two antiparallel four-stranded β-sheets, with the eight β-strands connected through six β-arches and one β-hairpin. The non-local character of the structure grows from the first β-arcade, which starts from the central β-hairpin, to the last one, where the N and C termini are paired.

The analysis from Fig. 1 leads to strong constraints on the construction of β-sheet backbone structures, as the side chain directionality patterns of the β-strands and loops are coupled in several ways. First, the directionality patterns of the loops preceding and following β-arcades confirm that the β-strands and loops are coupled in several ways. Second, the way in which it twists and bends the polypeptide chain, is associated with a specific flanking residue side chain pattern (Fig. 1b).

The most frequently observed turn types (between 1 and 5 amino acids) for each side chain pattern are listed in Fig. 1c; for example, BBG is strongly associated with the 1 | VOL 25 | NOVEMBER 2018 | 1028–1034 | www.nature.com/nsmb

| β-arch pattern | CuC[^\(\alpha\)][^\(\beta\)] \(\d\) > 0 | CuC[^\(\alpha\)][^\(\beta\)] \(\d\) < 0 |
|----------------|---------------------|---------------------|
| CuC[^\(\alpha\)][^\(\beta\)] \(\d\) > 0 | ↓↓ | ↓↓ |
| CuC[^\(\alpha\)][^\(\beta\)] \(\d\) < 0 | ↑↑ | ↑↑ |

**Fig. 1 | Constraints on β-arch geometry.** a, Side chain directionality in the β-arch. Comparison between β-hairpin and β-arch (left); the CxCβ and d vectors used to define the orientation of the two adjacent side chains are indicated. The four possible side chain directionality patterns are on the right. b, Turn type dependence of β-arc side chain patterns. Loops on the y axis are described by their ABEGO torsion bins (Supplementary Fig. 1). Most of the loops adopt only one of the four possible side chain patterns. c, Frequency of the most common loops for each of the four β-arch side chain patterns. There are strong preferences: for example, BBG is strongly associated with the ↑ pattern, whereas ABB is strongly associated with the ↓↓ pattern (bottom). Only loops with bending <120° (see Methods) and containing between 1 and 5 amino acids were considered in this analysis. d, β-arcades consist of two stacked β-arches with in-register strand pairing (left). Because strand pairs of the β-arcade are in register, the side chains adjacent to one β-arch loop must have the same orientation as the paired side chains that are adjacent to the second β-arch loop, and therefore not all loop pairs are allowed (middle). Example of a β-arcade formed by two common β-arches with compatible side chain patterns (right).
Fig. 2 | Double-stranded β-helix topology specification. a, The double-stranded β-helix fold consists of two four-stranded antiparallel β-sheets (in blue and green) with six β-arch and one β-hairpin connection. Pairs of β-arches forming the three β-arcades are highlighted (right). β-arch loops belonging to the same β-arcade are displayed with the same color throughout the figure (β-arcades 1, 2 and 3 in red, orange and magenta, respectively). b, Topology diagram of a designed double-stranded β-helix with all β-strand pairs in register. The Ca traces of the first and second β-sheets are colored in blue and green, respectively. Side chain CP positions oriented toward the inner and outer faces of the β-helix are represented with up and down black arrows with rounded tips, respectively. β-arc loops are colored as in a, c, Definition of β-arcade register shift varied during conformational sampling. The β-arcade register shift (between β-arcades 1 and 3) is determined by the register of β-strand pairs S3/S8 and S4/S7, and the lengths of β-strands S3, S4, S6 and S7 (see Methods). In this example, β-strand pairs S3/S8 and S4/S7 each have a two-residue register shift, resulting in an overall β-arcade register shift of four residues. Loops are omitted to facilitate visualization. d, Example of a design model with all β-strand pairs in register forming a sandwich-like structure. e, Example of a design model with register shifts between β-arcades 1 and 3 (magenta and red) forming a barrel-like structure.

Each β-strand are coupled to the length of the strand (Fig. 2b): for example, a β-strand with an even number of residues that is preceded by a ↑↑ loop must be followed by a ↓↑ or a ↓↓ loop, but not a ↑↓ or ↑↑ loop, owing to the alternating pleating of β-strands. Second, because the β-arcades of the β-helix have paired β-strands and β-arch loops, the side chains adjacent to one β-arch loop must have the same orientation as the paired side chains adjacent to the second β-arch loop (Fig. 1a). Owing to the antiparallel orientation of the β-arcades, ↑↓ and ↑↑ loops are compatible with loops of the same type, but ↑↓ loops are only compatible with ↑↑ loops (Fig. 1d). Third, the twist and curvature of the two β-sheets of the β-helix are constrained by the hydrogen-bonding register between β-arcades 1 and 3 (herein called β-arcade register), and within β-strand pairs S3/S8 and S4/S7, as shown in Fig. 2c.

De novo design of protein structures. We constructed double-stranded β-helix protein backbones by Monte Carlo fragment assembly using blueprints (representations of the target protein topologies specifying the ordering, lengths and backbone torsion bins of secondary structure elements and loop connections) in conjunction with backbone hydrogen-bonding constraints specifying all pairings between β-strands. We explored strand lengths between 5 and 7 residues and the most commonly observed β-arch loops between 3 and 5 residues (Fig. 1c). The central β-hairpin was designed with two-residue loops following the ββ rule. The register shifts between pairs of β-strands from different β-arcades (1 and 3) were allowed to range from 0 to 2 and the β-arcade register shifts between 0 and 4; strand pairs within the same β-arcade were kept in register. A total of 3,673 combinations were enumerated, of which 1,853 had mutually compatible strand lengths and loop types consistent with the constraints summarized in the previous paragraph. For each of these internally consistent blueprints, we used Rosetta to build thousands of protein backbones. The resulting ensemble of backbone structures has considerable structural diversity; those
with all strands in register had narrow, sandwich-like structures (Fig. 2d), while those with large register shifts had wider, barrel-like structures (Fig. 2e).

For each generated backbone, we carried out flexible-sequence design calculations to identify low-energy amino acid identities and side chain conformations providing close complementary packing, side chain–backbone hydrogen bonding in β-arch loops (to pre-organize their conformation and facilitate folding), and high sequence–structure compatibility. We favored inward-pointing charged or polar amino acids at the four edge strands to minimize aggregation propensity. Loop sequences were designed with consensus profiles obtained from fragments with the same backbone ABEGO torsion bins. Because the very large size of the space sampled by our design procedure limits convergence on optimal sequence–structure pairs, we carried out a second round of calculations starting from the blueprints yielding the lowest-energy designs, intensifying sampling at both the backbone and sequence level. For a subset of designs, we introduced disulfide bonds between paired β-strand positions with high sequence separation (for example, between the first and last β-strands) and optimal orientation (see Methods): disulfide bonds distant in primary sequence decrease the entropy of the unfolded state and therefore enhance the thermodynamic stability of the native state. To assess compatibility of the top-ranked designed sequences with their structures, we characterized their folding energy landscape with biased forward folding simulations, and those with substantial near-native sampling were subsequently assessed by Rosetta ab initio structure prediction calculations. Designs with funnel-shaped energy landscapes (where the designed structure is at the global energy minimum and has a substantial energy gap with respect to alternative conformations) were selected for experimental characterization. Ab initio structure prediction of natural β-sheet proteins tends to oversample structure prediction of natural β-sheet proteins, and Supplementary Fig. 3). For both designs, the number of NMR samples by size-exclusion chromatography coupled with multi-angle light scattering (SEC-MALS) (most of the non-monomeric designs had far-ultraviolet circular dichroism spectra (CD) at 25°C characteristic of β-strands, but this did not succeed in yielding stable monomers.

Addition of an α-helix to the C terminus (one of the two extremes of the β-helix), as a capping domain protecting the strand edges from intermolecular pairing, also failed to yield stable monomers, even in combination with disulfide bonds. This suggests that the sequence of the core β-sheet must strongly encode its structure independently of disulfide bonds or protecting domains aimed at increasing stability.

**Experimental characterization.** For experimental characterization, we chose 19 designs with funnel-shaped energy landscapes ranging between 70 and 94 amino acids (Supplementary Table 1). BLAST searches indicated that the designed sequences had little or no similarity with native proteins (lowest Expect (E) values ranging from 0.003 to >10; Supplementary Table 2). Synthetic genes encoding the designs (design names are BH_n, where BH stands for β-helix, n stands for the design number and the _ss suffix is used if disulfide bonds are present) were obtained; the proteins were expressed in Escherichia coli and purified by affinity chromatography. Sixteen of the designs expressed well and were soluble, and two (BH_10 and BH_11) were monomeric (Supplementary Fig. 2) by size-exclusion chromatography coupled with multi-angle light scattering (SEC-MALS) (most of the non-monomeric designs were either dimers or soluble aggregates). Both monomeric designs had far-ultraviolet circular dichroism spectra (CD) at 25°C characteristic of β proteins, a melting temperature (Tm) above 95°C, and well-ordered structures according to 2D 1H-15N heteronuclear single-quantum coherence (HSQC) spectra (Fig. 3a–c and Supplementary Fig. 3). For both designs, the number of NMR peaks matched the number of expected amide resonances based on the protein sequence, but the higher stability of BH_10 under the conditions of the NMR experiments made it a better candidate for NMR structure determination.

The two monomeric designs with well-ordered structures were among those with better-packed cores and a larger proportion of β-arch loops containing prolines and with backbone polar atoms making hydrogen bonds (Supplementary Table 3). β-arch loops that are structurally preorganized with the polar groups making internal hydrogen bonding likely favor folding to the correct topology and contribute to stability by compensating for the loss of interactions with water of polar groups in the side chains and backbone. These interactions likely disfavor the competing local strand-pairing arrangement in which the two strands form a β-hairpin; this is a very common pathology in ab initio structure prediction. For the most stable dimeric design (BH_6), we introduced disulfide bonds to stabilize protein regions having contacts with large sequence separation (for example, between the N- and C-terminal strands), but this did not succeed in yielding stable monomers. Addition of an α-helix to the C terminus (one of the two extremes of the β-helix), as a capping domain protecting the strand edges from intermolecular pairing, also failed to yield stable monomers, even in combination with disulfide bonds. This suggests that the sequence of the core β-sheet must strongly encode its structure independently of disulfide bonds or protecting domains aimed at increasing stability.

**NMR structure of a de novo–designed β-helix.** We succeeded in solving the structure of BH_10 by 4D NMR spectroscopy (Fig. 3d, Table 1 and Supplementary Fig. 4), using the 4D-CHAINs/AutoNOE-Rosetta automated pipeline for resonance assignments and structure calculation, and found it to be in very close agreement with the computational model (Cα r.m.s. deviation (r.m.s.d.) of 0.84 Å, averaged over 10 NMR models). The overall topology is accurately recapitulated, including all strand pairings, register shifts and loop connections, as supported by 132 long-range nuclear Overhauser effects (NOEs) between backbone amide and side chain protons (Supplementary Fig. 5). The designed aliphatic and aromatic side chain packing in the protein core, as well as salt bridge interactions across the two β-sheet surfaces, was also accurately reproduced; three salt bridges between the two paired β-arcades and one within the third β-arcade are well supported by the observed NOEs (Supplementary Fig. 6). The agreement in both the backbone conformation and hydrogen-bonding interactions of the loops forming the three β-arcades is remarkable given that these elements are the most flexible parts of the structure and therefore difficult to design owing to sampling bottlenecks. The β-arcades were designed with pairs of β-arch loops that interact via backbone-backbone hydrogen bonds (owing to the complementarity between their backbone conformations) stabilizing loop pairing and avoiding burial of polar backbone atoms (see Supplementary Fig. 7 for the BH_10 loop sequences and side chain patterns). For example, β-arcade 1 is formed by BBG and ABB loops, and the buried backbone NH group of the G position in the former makes a hydrogen bond with the buried backbone C=O of the neighboring loop (Fig. 3e). The other two β-arcades were designed with one β-arch loop containing buried and fully hydrogen-bonded asparagines (four hydrogen bonds in total) that stabilize both loop pairing and the local β-arch conformation (of ABABB loops). By design, the asparagine side chain geometry was further stabilized with hydrophobic stacking interactions from the two β-arch loops of the same arcade. The high degree of convergence of the designed rotamer in the NMR ensemble illustrates the high structural preorganization of this particular motif (Fig. 3f).

The amino acid sequence of BH_10 is unrelated to any sequence in the NCBI nr database (BLAST found one hit with insignificant sequence similarity; E value 6.3). We searched the Protein Data Bank (PDB) for similarities in structure (using the Dali server with the lowest-energy NMR model as the query structure) or sequence (with HHpred for sensitive profile-based sequence search), and identified matches similar in fold but containing additional and irregular secondary structures and longer loops. These matches are all homodimers with sheet-to-sheet interface packing (Supplementary Fig. 8) or domains integrated in larger structures, in sharp contrast to the BH_10 monomer.
Contact order and sequence determinants of the BH_10 fold. The non-local character of BH_10 is of particular note: a large fraction of the contacting residues are distant along the linear sequence, with extensive strand pairing between the N- and C-terminal β-strands. The contact order of the structure (that is, the average separation along the linear sequence of residues in contact in the 3D structure) is higher than that for any previous single-domain protein designed de novo (Fig. 3g,h). Proteins with high contact order fold more slowly than those with low contact order as there is a greater loss in chain entropy for forming the first native interactions, and they tend to form long-lived non-native structures that can oligomerize or aggregate. We have overcome the challenges in designing...
We have successfully designed a double-stranded β-helix de novo, as confirmed by the NMR structure of the design BH_10, based on a series of rules describing the geometry of β-arch loops and their interactions in more complex β-arcades. Our work also achieves two related milestones: the first accurate design of an all-β globular protein with exposed β-sheet edges, and the most non-local structure yet designed from scratch. Comparison of successful and failed designs suggests that folding and stabilization of the monomeric structure (and implicitly disfavoring competing topologies with more local strand pairings) is bolstered by loops containing side chain–backbone and backbone-backbone hydrogen bonds together with well-packed mixed aliphatic/aromatic side chains in the protein core, inward-pointing polar amino acids at strand edges and salt bridges between paired strands. Previous design studies on β-propellers or parallel β-helices have used naturally occurring backbone structures and consensus sequence information on the target fold families; this approach, while powerful, sheds less light on the key principles underlying β-sheet structure construction and does not allow the programming of new backbone geometries. The β-helix fold designed here is well suited for incorporating metal, ligand-binding and active sites, as illustrated by the broad functional diversity of cupin protein domains, which are the closest naturally occurring structural analogs. With the basic design principles now understood, our de novo design strategy should enable the construction of a wide range of β-helix structures tailored to a broad range of target ligands.

Initial advances in protein design were from algorithms that allowed rapid identification of a very-low-energy sequence for a given backbone structure. In recent years, progress has come from the realization that the requirements of burying hydrophobic residues in a core away from solvent while avoiding the burial of backbone polar groups without compensating hydrogen bonds, together with torsional restrictions on the peptide backbone, considerably constrain overall globular protein backbone geometry, particularly for β-sheet-containing proteins: it is much harder than originally expected to construct new backbones that have these properties. The de novo design of β-sheet-containing proteins advanced considerably following the elucidation of β-sheet design principles for construction of backbones meeting the above constraints while having desired geometries: for example, principles for controlling the chirality of β-hairpins, reducing strain in β-strands with glycine kinks and combining β-bulges and register shifts to curve β-sheets. The design rules described here are a considerable further advance as they provide control over β-arch connections between distinct β-sheets, and should enable the design of a broad range of β-protein families beyond the β-barrel and β-helix, with considerable medical and biotechnological potential; for example, the immunoglobulin fold widely utilized for binding and loop scaffolding in nature is topologically very similar to the double-stranded β-helices designed here, with a larger proportion of β-hairpins over β-arches.

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Table 1 NMR and refinement statistics for BH_10

| NMR distance and dihedral constraints | BH_10 (PDB 6E5C) |
|---------------------------------------|------------------|
| Distance constraints                  |                  |
| Total NOE                             | 659              |
| Intraresidue                          | 272              |
| Inter-residue                         | 387              |
| Sequential (|i| - |j| = 1)                      | 222              |
| Medium range (2 ≤ |i| - |j| ≤ 4)                    | 33               |
| Long range (|i| - |j| ≥ 5)                       | 132              |
| Intermolecular                        | 0                |
| Hydrogen bonds                        | 0                |
| Total dihedral angle restraints       | 156              |
| Violations (mean ± s.d.)              |                  |
| Distance constraints (Å)              | 0.30 ± 0.46      |
| Dihedral angle constraints (°)        | 9.30 ± 2.49      |
| Max. dihedral angle violation (°)     | 47.59            |
| Max. distance constraint violation (Å)| 1.32             |
| Deviations from idealized geometry    |                  |
| Bond lengths (Å)                      | 0.00 ± 0.00      |
| Bond angles (°)                       | 0.00 ± 0.00      |
| Improper (°)                          | 0.00 ± 0.00      |
| Average pairwise r.m.s.d. (Å)         | 0.61 ± 0.13      |
| Heavy                                 |                  |
| Backbone                              | 0.51 ± 0.11      |

*a*Distance constraint violations in the structural ensemble were calculated using a 7-Å universal upper distance bound for the NOE restraints assigned by AutoNOE-Rosetta. *b*Dihedral angle restraints were derived from TALOS-N. The violations were calculated for the core secondary structural regions of the ten lowest-energy models using a 15° cutoff beyond TALOS-N-predicted dihedral angles. *c*Pairwise r.m.s.d. was calculated among ten refined models for a core secondary structural region defined by residues 2-8, 11-18, 21-28, 32-36, 39-43, 46-53, 59-65 and 71-75.
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Author contributions

E.M. designed the research, carried out the loop structural analysis, set up the design method and performed design calculations. T.M.C. carried out design calculations, protein expression, purification and CD experiments. A.C.M. collected 4D NMR data. T.E. performed 4D-CHAINS analysis. L.C. expressed isotopically labeled proteins and performed SCEL-MALS analysis. L.G.N. designed the research and carried out design calculations. A.D. and G.O. helped in protein expression and characterization. K.T. and N.G.S. supervised NMR structure determination. D.B. designed and supervised the research. E.M., and D.B. prepared the manuscript with input from all authors.

Competing interests

The authors declare no competing interests.

Additional information

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Further restrictions were imposed to improve sequence-structure compatibility in hydrophobic amino acids were located in the core and polar ones in the surface. were restricted based on the solvent accessibility of protein positions, ensuring that flexible-sequence design calculations with RosettaDesign18,19 using the Rosetta Generated protein backbones were subjected to atom flexible-sequence design (see next section).

Methods

Loop analysis. Loop connections between β-strands were collected from a non-redundant database of PDB structures obtained from the PISCES server17 with sequence identity <30% and resolution ≤2 Å. We discarded those loops connecting β-strands with hydrogen-bonded pairing (β-hairpins), and the remaining 5,000 β-arch loops were subsequently analyzed. The ABEGO torsion bins of each residue position were assigned based on the definition shown in Supplementary Fig. 1, and the side chain directionality pattern of neighboring residues was defined according to Fig. 1a. The secondary structure of all residue positions was assigned with DSSP20 and the last β-strand residue preceding and the first β-strand residue following the β-arch loop were chosen as the critical neighboring residues determining the side chain pattern of the loop. The loop bending was defined as the angle between the loop center of mass and the two strand positions adjacent to the loop. Those loops with bending angles larger than 120° were discarded from the analysis to correctly identify those loops producing a substantial change in the direction of the two connected β-strands. The loop dataset is available in Supplementary Dataset 2.

Backbone generation. We used the Blueprint Builder mover10 of RosettaScripts14 to build protein backbones by Monte Carlo fragment assembly using nine- and three-residue fragments compatible with the target secondary structure and torsion bins (ABEGO), as specified in the blueprints of every target topology. We used a polyvaline centroid representation of the protein and a scoring function accounting for backbone hydrogen bonding, van der Waals interactions (namely to avoid steric clashes), planarity of the peptide bond (omega score term), and compactness of structures (radius of gyration). Thousands of independent folding trajectories were performed and subsequently filtered. Owing to the non-local character of β-sheet contacts, we used distance and angle constraints to favor the correct hydrogen-bonded pairing between β-strand main chain atoms. For every target topology, we automatically set all pairs of residues involved in β-pairing to generate all constraints for backbone building. Protein backbones were filtered based on their match with the blueprint specifications (secondary structure, torsion angle, strand pairing), and subsequently ranked based on backbone hydrogen-bonding energy (lr, hb score term) and the total energy obtained from one round of all-atom flexible-sequence design (see next section).

Flexible-sequence design. Generator generated backbone proteins were subjected to flexible-sequence design calculations with RosettaDesign18 using the Rosetta all-atom energy function Talaris201414 to favor amino acid identities and side-chain conformations with low energy and tight packing. We performed cycles of fixed backbone design followed by backbone relaxation using the FastDesign mover10 of RosettaScripts14. Designed sequences were filtered based on total energy, side-chain packing (measured with RosettaHolés16, packstat and core side-chain average degree17), side-chain backbone hydrogen bond energy, and secondary structure prediction (match between the designed secondary structure and that predicted by PI-SIPRED18 based on the designed sequence). Amino acid identities were restricted based on the solvent accessibility of protein positions, ensuring that hydrophobic amino acids were located in the core and polar ones in the surface. Further, we restricted the bending angle of β-strands in loop regions. Sequence profiles were obtained for naturally occurring loops with the same ABEGO string sequence, as previously19.

For those blueprints that yielded the lowest energy designs we performed a second round with ten times more backbone samples. Backbones generated in this second round were subjected to more exhaustive sequence design by running multiple Generic Monte Carlo trajectories optimizing total energy and side chain average degree simultaneously, and then applied all filters described above.

Design of disulfide bonds and helix capping domain. We used the Disulfide mover of RosettaScripts14 to identify pairs of residue positions able to form disulfide bonds with a good scoring geometry. We searched for disulfide bonds between residues distant in primary sequence and with a disulphide score <1.0. We designed a C-terminal helix capping domain (followed with a β-strand pairing with the first β-strand) using the backbone-generation protocol described above but starting from design BH_6. The structure of BH_6 was kept fixed during fragment assembly and the C-terminal domain was generated. Then, sequence design was performed for the C-terminal domain and those neighboring residues with a ±10 Å.

Sequence-structure compatibility. For assessing the local compatibility between designed sequences and structures we picked 200 naturally occurring fragments (9- and 3-mers) with sequences similar to the design, and evaluated the structural similarity between the ensemble generated with the ensemble fragment library and the local designed structure. Those with low r.m.s.d. fragments, and therefore with high fragment quality, were subsequently assessed by Rosetta folding simulations using the Roseta energy function ‘ref2015’14. First, biased forward folding simulations (“using the three lowest r.m.s.d. fragments and 40 folding trajectories) were used to quickly identify those designs more likely to have funnel-shaped energy landscapes and those designs achieving near-native sampling (r.m.s.d. to target structure below 1.5 Å) were then assessed by standard Rosetta ab initio structure prediction17,21.

To evaluate the amount of β-hairpin sampling in each loop connection during ab initio structure prediction, we first detected all strand pairings formed in each generated decoy and then mapped the residues involved in those strand pairings to the secondary structure elements of the designed structure. After secondary structure mapping, pairings between strands consecutive in the sequence were counted as β-hairpins. The total count of β-hairpins sampled in each loop over the total number of generated decoys is a relative quantity of hairpin sampling allowing us to compare the β-hairpin propensity of different loops and mutants (see Supplementary Fig. 9).

Contact order. To evaluate the non-local character of protein structures we computed ‘contact order’ as the average sequence separation between pairs of Ca atoms within a distance of 8 Å and with a sequence separation of three residues at least.

Protein expression and purification. Genes encoding the designed sequences were obtained from Genscript and cloned into the pET-28b+ (with N-terminal 6x His tag and a thrombin cleavage site) expression vectors. Plasmids were transformed into Escherichia coli BL21 Star (DE3) competent cells, and starter cultures were grown at 37 °C in LB medium overnight with kanamycin. Overnight cultures were used to inoculate 500 ml LB medium supplemented with antibiotic, and cells were grown at 37 °C and 225 r.p.m. until an optical density (OD600) of 0.5–0.7 was reached. Protein expression was induced with 1 mM IPTG at 18 °C and, after overnight expression, cells were collected by centrifugation (at 4 °C and 4,400 r.p.m. for 10 min) and resuspended in 25 ml of lysis buffer (20 mM imidazole and PBS). Resuspended cells were lysed in the presence of lysozyme, DNase and EDTA and centrifuged at 4°C and 18,000 r.p.m. for 30 min, and the supernatant was loaded onto a nickel affinity gravity column pre-equilibrated in lysis buffer. The column was washed with three column volumes of PBS+30 mM imidazole and the purified protein was eluted with three column volumes of PBS+250 mM imidazole. The eluted protein solution was dialyzed against 1.5 l buffer overnight. The expression of purified proteins was assessed by SDS–PAGE and mass spectrometry, and protein concentrations were determined from the absorbance at 280 nm measured on a NanoDrop spectrophotometer (Thermo Scientific) with extinction coefficients predicted from the amino acid sequences using the ProtParam tool (https://web.expasy.org/protparam/). Proteins were further purified by fast protein liquid chromatography size-exclusion chromatography using a Superdex 75 10/300 GL (GE Healthcare) column.

Circular dichroism. Far-ultraviolet CD measurements were carried out on the AVIV 420 spectrophotometer. Wavelength scans were measured from 260 to 195 nm at temperatures between 25 and 95 °C, using a 1-mm path-length cuvette. Protein samples were prepared in PBS buffer (pH 7.4) at a concentration of 0.2–0.4 mg ml⁻¹.

Size-exclusion chromatography combined with multiple-angle light scattering. SEC-MALS experiments were performed using a Superdex 75 10/300 GL (GE Healthcare) column combined with a miniDawn TREFOS multi-angle static light scattering detector and an Optilab T-REX refractometer (Wyatt Technology). One-hundred-microliter protein samples were injected into a 500-µl column equilibrated with PBS (pH 7.4) or TBS (pH 8.0) buffer at a flow rate of 0.5 ml min⁻¹. The collected data were analyzed with ASTRA software (Wyatt Technology) to estimate the molecular weight of the eluted species.

Protein expression of isotopically labeled proteins for NMR structure determination. Plasmids were transformed using standard heat-shock transformation into the Lemo21 expression strain of Escherichia coli (NEB) and plated onto a minimal M9 medium containing glucose and kanamycin to maintain tight control over expression. A single colony was selected, inoculated into 50 ml of LB containing 50 µg ml⁻¹ of kanamycin and grown at 37 °C with shaking overnight. After approximately 18 h, the 50-ml starter culture was removed and 25 ml was used to inoculate 500 ml of Terrific Broth (TB) containing 50g ml⁻¹ kanamycin and mixed mineral salts16. The TB culture was grown at 37 °C with shaking at 250 r.p.m. until the OD600 reached a value of 1.0. Then, the culture was removed and the cells were pelleted by centrifugation at 4,000 r.p.m. for 15 min. The TB broth was removed and the pelleted cells were resuspended gently with 50 ml of 20 mM NaPO4, 150 mM NaCl, pH 7.5. The resuspended cells were transferred into minimal labeling media, containing 15N-labeled ammonium chloride at 50 mM and 13C-labeled glucose to 0.25% (w/v), as well as trace metals, 25 mM NaHPO4, 25 mM KH2PO4 and 5 mM Na2SO4. The culture was returned to 37 °C at 250 r.p.m. for 1 h in order to replace unlabeled nitrogen and carbon with labeled nitrogen and carbon, respectively. After 1 h, IPTG was added to a final concentration of 1 mM and the culture was allowed to express overnight. The following morning, the culture was removed and the cells were pelleted by centrifugation at 4,000 r.p.m. for 15 min. The cells were resuspended with 40 ml of lysis buffer (20 mM Tris, 250 mM NaCl, 0.25% CHAPS, pH 8) and lysed with a Microfluidics M110P Microfluidizer at 18,000 p.s.i. The lysed cells were clarified using centrifugation at 24,000g for 30 min. The labeled protein in the soluble fraction was then immobilized metal affinity chromatography using standard methods (Qlagen Ni-NTA resin). The purified protein was then concentrated to 2 ml and purified by FPLC.
BH_10 target protein, we obtained NMR chemical shifts from 4D-CHAINs28 and fragments, chemical shifts and unassigned NOESY cross-peak lists. For the steps, AutoNOE-Rosetta calculations are set up with target sequence, structural (3) the predicted secondary structure, together with trimmed chemical shift files because they cause deterioration of the performance of structure calculation. HSQC experiments were acquired at 37 °C with four scans, acquisition times of 72 ms (N) in the indirect dimension and recycle delay of 2 s. Chemical shift assignment. For chemical shift assignment of BH_10, a set of two non-uniformly sampled (NUS) 4D NMR experiments, a 4D HC(CC-TOCSY(CO)) dimension (0.32% sparsity). 4D NUS spectra were processed in NMRPipe41 using SMILE reconstruction42 and analyzed using NMRPipe-Sparky43. For every H-1N HSQC, the corresponding peaks in 4D HCCH-TOSY and 4D-HCNH NOESY spectra were inspected and peaks were picked manually. The 4D peak lists were used as input for the 4D-CHAINs algorithm28 to obtain sequence-specific resonance assignments of backbone and side chain atoms automatically. The overall assignment completeness with achieved 92% of aromatic resonances were assigned. 4D-CHAINs assignments together with the 4D-HCNH NOESY peak list were used in AutoNOE-Rosetta for structure determination.

NOE assignment and structure determination using AutoNOE-Rosetta. To determine the structural models of the BH_10 target protein, we used CS-Rosetta37 that provides AutoNOE-Rosetta36 and RASREC-Rosetta34 protocols. AutoNOE-Rosetta is an iterative NOE assignment method that utilizes RASREC-Rosetta to model protein structures de novo. These methods make use of valuable information contained within NMR chemical shifts about secondary and tertiary structures, and dynamics of proteins, to model targets of interest accurately43. The primary aim of AutoNOE-Rosetta is to label proton to the unassigned NOESY cross-peaks by mapping their resonance frequencies to the assigned chemical shift frequencies. These assignments can be utilized to generate NOE-based distance restraints that aid the structure calculation process. The method begins by creating an initial mapping between the assigned chemical shift list and the unassigned NOESY cross-peak list. This mapping produces ambiguous assignments due to possible noise in the NOESY spectra36. These assignments undergo additional filtering during the calculation. The primary criterion is that the NOE-based distance restraints that aid the structure calculation process. The process of setting up AutoNOE-Rosetta calculations is highly automated and accessible via a Python interface within the toolbox available at the CS-Rosetta website (https://crossetta.chemistry.ucsd.edu). Before setting up NOE assignment and structure calculation runs, (1) NMR chemical shifts and target sequences are used to predict secondary structure (rigid regions) and flexible regions from the NOESY spectra and the contribution to some of the evaluation criteria (such as network anchor score) is insignificant. The intensities of high-scoring NOE peaks are calibrated to produce distance restraints. These restraints are used to calculate structures within the highly parallel RASREC-Rosetta, which performs fragment assembly54 using Monte Carlo methods and additional optimization algorithms55. This process of assigning NOEs and calculating structures is carried out iteratively across eight distinct stages. The final stage retains the highest-scoring structure, and the final model is the lowest-energy structure that has been deposited in the protein database.

Data availability. NMR chemical shifts and NOESY cross-peaks lists used to determine structures of BH_10 have been deposited in the BMRB with accession code 30495. Coordinates of the ten lowest-energy structures and the restraint lists have been deposited in the wwPDB as PDB 6E5C. The design model of BH_10 is available as Supplementary Dataset 2. The loop datasets used to analyze the side chain patterns of naturally occurring β-chains are available in Supplementary Dataset 2. Other data are available from the corresponding authors upon reasonable request.

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- Protein structures used for loop geometric analysis were obtained from a non-redundant database of natural proteins from the Protein Data Bank.

Data analysis

- Analyses on protein structures were carried out with PyRosetta and all design and folding calculations were done with Rosetta. All NMR analyses were done as described in the methods section with the following programs: NMRPipe, NMRFAM-SPARKY, 4D-CHAiNS, CS-Rosetta and TALOS-N.
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NMR chemical shifts and NOESY cross-peak lists used to determine structures of B&H_10 have been deposited under BMRB ID 30495. Coordinates of ten lowest-energy structures and the restraint lists have been deposited under the PDB ID 6E5C.

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