Ab initio study of compressed Ar(H$_2$)$_2$: structural stability and anomalous melting

Claudio Cazorla$^a$ and Daniel Errandonea$^b$

$^a$ Department of Chemistry, University College London, London WC1H 0AJ, United Kingdom
$^b$ Departamento de Física Aplicada -ICMUV-, Fundació General Universitat de València, Spain

We study the structural stability and dynamical properties of Ar(H$_2$)$_2$ under pressure using first-principles and ab initio molecular dynamics techniques. At low temperatures, Ar(H$_2$)$_2$ is found to stabilize in the cubic C15 Laves structure (MgCu$_2$) and not in the hexagonal C14 Laves structure (MgZn$_2$) as it has been assumed previously. Based on enthalpy and phonon calculations, we propose a temperature-induced MgCu$_2$ → MgZn$_2$ phase transition that may rationalize the existing discrepancies between the sets of Raman and infrared vibron measurements. Our AIMD simulations suggest that the melting line of Ar(H$_2$)$_2$ presents negative slope in the interval 60 ≤ P ≤ 110 GPa. We explain the origin of this intriguing physical phenomenon in terms of decoupling of the Ar and H$_2$ degrees of freedom and effective thermal-like excitations arising from coexisting liquid H$_2$ and solid Ar phases.

PACS numbers: 31.15.A-, 64.70.K-, 81.30.-t, 64.70.dj

I. INTRODUCTION

Solid hydrogen H$_2$ is expected to become metallic at compressions higher than 400 GPa [1]. In fact, experimental signatures of the long-sought insulator-to-metal phase transition remain elusive up to pressures of ~340 GPa [2]. Accepted pressure-induced mechanisms by which the metallicity of hydrogen can be enhanced involve atomization of H$_2$ molecules and partial filling of electronic $\sigma^*$ molecular levels due to charge transfer from or band hybridization with other chemical species [2,3]. Already in the earlier 90’s Loubeyre et al., based on the disappearance of the Raman (R) vibron mode and the darkening of the material, claimed to observe metatllization of the Ar(H$_2$)$_2$ compound when compressed in the diamond-anvil-cell (DAC) up to ~200 GPa [3]. The stable room-temperature (RT) phase structure of this compound was identified with the hexagonal C14 Laves structure typified by the MgZn$_2$ crystal (space group: P6$_3$/mmc). Strikingly, posterior synchrotron infrared (IR) measurements did not show evidence of molecular bonding instabilities nor metallic Drude-like behavior up to at least 220 GPa [6]. Subsequently, Bernard et al. suggested that activation of H$_2$ dissociation processes and corresponding development of metallization in Ar(H$_2$)$_2$ could occur via a solid-solid phase transition of the MgZn$_2$ → AlB$_2$ (space group: P6$_3$/mmc) type at pressures already within the reach of DAC capabilities [7]. However, recent ab initio work done by Matsumoto et al. demonstrates that the onset of metallicity in the AlB$_2$ structure commences at pressures significantly higher than in pure bulk H$_2$ [8].

In view of the growing interest on hydrogen-rich van der Waals (vdW) compounds under pressure [10], partly motivated by the hydrogen-storage problem, and of the unresolved discrepancies described above, we have conducted a theoretical study on Ar(H$_2$)$_2$ under extreme P − T conditions using first-principles density functional theory (DFT) calculations and ab initio molecular dynamics simulations (AIMD). In this letter, we present results showing that at low temperatures and pressures up to ~215 GPa the Ar(H$_2$)$_2$ crystal stabilizes in the cubic C15 Laves structure typified by the MgCu$_2$ solid (space group: Fd$\bar{3}$m). This structure has not been considered in previous works [7,10] though its probable relevance to Ar(H$_2$)$_2$ was pointed out recently [11]. On the light of first-principles enthalpy and phonon calculations, we propose a temperature-induced (pressure-induced) phase transition of the MgCu$_2$ → MgZn$_2$ (MgZn$_2$ → MgCu$_2$) type that may clarify the origin of the discrepancies between the sets of R and IR data. Furthermore, in the high-P regime (P ~ 210 GPa) we find that a metallic hydrogen-rich liquid can be stabilized at temperatures of ~4000 K wherein H-H coordination features render molecular dissociation activity. By means of AIMD simulations, we estimated an upper bound of the melting curve P(T$_m$) of Ar(H$_2$)$_2$ and found a negative $\partial T_m/\partial P$ slope spanning over the interval 60 ≤ P ≤ 110 GPa. Our simulations show that the lattice composed by H$_2$ molecules melts at temperatures significantly lower than the lattice of Ar atoms does, so leading to stable mixtures of coexisting liquid H$_2$ and solid Ar over wide P − T ranges. We propose an argument based on this atypical physical behavior to explain the cause of the estimated negative $\partial T_m/\partial P$ slope.

II. OVERVIEW OF THE CALCULATIONS

Our calculations were performed using the all-electron projector augmented wave method and generalized gradient approximation of Wang and Perdew as implemented in the VASP code [12]. Dense Monkhorst-Pack special k-point meshes [13] for sampling of the first Brillouin zone (IBZ) and a cutoff energy of 400 eV were employed to guarantee convergence of the total energy per particle to within 0.5 meV. In particular, we used 8 × 8 × 8, 8 × 8 × 4 and 12 × 12 × 12 k-point grids for calculations on the perfect unit cell corresponding to the MgCu$_2$, MgZn$_2$ and AlB$_2$ crystal structures, respectively. All
the considered crystal structures were relaxed using a conjugate-gradient algorithm and imposing the forces on the particles to be less than 0.005 eV/Å. The phonon frequencies in our calculations were obtained using the small-displacement method \cite{14} over the unit cells (Γ-point phonon frequencies) and large supercells containing 80 atoms. \textit{Ab initio} molecular dynamics simulations were carried out in the canonical ensemble \((N, V, T)\) using bulk supercells of \(\text{Ar(H}_2)_2\) containing 160 atoms (Γ-point sampling). At given pressure, the dynamical properties of the system were sampled at 400 K intervals from zerotemperature up to the melting curve of pure Ar. Temperatures were maintained using Nosé-Hoover thermostats. A typical AIMD simulation consisted of 3 ps of thermalization followed by 7 ps over which statistical averages were taken. It is worth noticing that we recently used a very similar computational approach to the one described here to study the energetic and structural properties of \(\text{Ar(He)}_2\) and \(\text{Ne(He)}_2\) crystals under pressure \cite{11}, and that very recent experiments \cite{16} have confirmed the validity of our predicted \(P(V)\) curves.

III. RESULTS AND DISCUSSION

A. \textit{Low-}\(T\) results

A series of candidate structures were considered in our \textit{ab initio} enthalpy \(H(P)\) calculations ( Rutile, Fluorite, MgNi\(_2\), etc.) however only the MgZn\(_2\), MgCu\(_2\) and AlB\(_2\) structures turned out to be energetically competitive so the following analysis concentrates on these ones. Ignoring quantum zero-point motion effects, we found that \(\text{Ar(H}_2)_2\) is energetically more stable in the MgCu\(_2\) structure than in either the MgZn\(_2\) or AlB\(_2\) structures at pressures \(P \leq 215\) GPa (see Figure 1). Also we predicted that at \(P_t = 215(1)\) GPa the solid transitates from the MgCu\(_2\) to the AlB\(_2\) structure. The calculated zero-temperature equation of state of \(\text{Ar(H}_2)_2\) in the MgCu\(_2\) structure displays very good agreement with respect to the available experimental data \cite{7} (see Figure 2). For instance, at \(V = 14.61\) and 12.50 Å\(^3\)/particle we obtain a pressure of 8.83 and 17.14 GPa, respectively, to be compared with the experimental values 8.77 and 15.79 GPa. It must be noted that the estimated equation of state and pressure-dependence of the H-H intermolecular bond distance of the MgZn\(_2\) and MgCu\(_2\) phases appear to be indistinguishable within the numerical uncertainty in our calculations (namely, 1 GPa and 0.01 Å-see Figure 2).

Since hydrogen is a very light molecule, quantum zero-point motion corrections must be included in the calculations. Customarily this is achieved using quasi-harmonic approaches that involve estimation of the vibrational phonon frequencies. In following this procedure, we found that \(\text{Ar(H}_2)_2\) in the MgZn\(_2\) structure always exhibits imaginary Γ-phonon frequencies at pressures below \(\sim 300\) GPa. This means that the MgZn\(_2\) structure is mechanically unstable, at least, at low temperatures. On the other hand, we found that the MgCu\(_2\) structure is perfectly stable at all the studied pressures. Our numerical tests showed that this result does not depend on the approximation of the exchange-correlation functional used \cite{15}. In Figure 3 we show the phonon frequency spectra of \(\text{Ar(H}_2)_2\) in the MgCu\(_2\) crystal structure calculated along a \(k\)-point path contained within the IBZ and
at pressure $\sim 200$ GPa.

Since the x-ray resolved RT crystal structure of Ar(H$_2$)$_2$ is MgZn$_2$ \cite{3}, we carried out a series of AIMD simulations of this and the MgCu$_2$ structure at $T = 300$ K in order to explore their stability. In fact, analysis of our simulations based on estimation of the averaged mean-squared displacement and position-correlation function \cite{18} showed that both MgCu$_2$ and MgZn$_2$ structures are mechanically stable at RT. On view of these results and the reported x-ray data, we concluded that a temperature-induced MgCu$_2$ $\rightarrow$ MgZn$_2$ transition occurs at fixed $P$ (or equivalently, a pressure-induced MgZn$_2$ $\rightarrow$ MgCu$_2$ transition at fixed $T$ - see Figure 1\textendash ). This temperature-induced transformation can be understood in terms of entropy: Ar(H$_2$)$_2$ in the MgZn$_2$ structure is highly anharmonic so ionic entropy contributions to the total free-energy stabilize this structure over the MgCu$_2$ phase with raising temperature. In fact, IR measurements displayed an splitting of the vibron mode in the interval $35 \leq T \leq 150$ K \cite{19}. This splitting can be induced by the degeneracy removal of the infrared E$_{1u}$ mode due to the decrease of the crystal quality caused by precursor effects of the MgZn$_2$ $\rightarrow$ MgCu$_2$ transition.

The causes of the aforementioned R-IR experimental disagreements can be rationalized in the light of the foreseen MgCu$_2$ $\rightarrow$ MgZn$_2$ transition, as we explain in what follows. In Figure 3, we enclose the calculated R and IR vibron frequencies of Ar(H$_2$)$_2$ in the MgZn$_2$, MgCu$_2$ and AlB$_2$ structures as function of pressure. At high pressures, it is shown that the A$_{1g}$ (R) vibron line corresponding to the MgZn$_2$ and MgCu$_2$ structures are practically identical, whereas they settle appreciably below the line estimated for the AlB$_2$ structure, and follow closely the low-$T$ R results \cite{3}. These outcomes together with the energy and phonon results already presented, led us to think that the sudden dissappearance of the R vibron mode observed at high-$P$ might be related to the MgCu$_2$ $\rightarrow$ MgZn$_2$ transition unravelled in this Letter and not to pressure-induced metallic-like behavior \cite{3} or MgZn$_2$ $\rightarrow$ AlB$_2$ phase transition \cite{7} as previously suggested. In fact, accurate electronic density of states (DOS) analysis performed on the perfect MgZn$_2$, MgCu$_2$ and AlB$_2$ crystal structures show no closure of the electronic band gap up to compressions of at least 420 GPa. Furthermore, the E$_{1u}$ (IR) vibron line that we calculated for the MgZn$_2$ structure at high pressures; according to our predictions, the vibron signature will eventually disappear at the crossing with the MgCu$_2$-MgZn$_2$ phase boundary since IR vibron modes in the MgCu$_2$ structure are inactive.

\subsection{High-$T$ results}

An intriguing physical phenomenon has been recently predicted and subsequently observed in H$_2$ under pressure. It consists in the appearance of a maximum peak on its melting line followed by a negative $\partial T_m/\partial P$ slope \cite{20,21}. This phenomenon have been explained in terms of subtle changes on the intermolecular forces due to compression instead of more familiar arguments like promotion of valence electrons to higher energy orbitals.
or occurrence of molecular dissociation processes. Motivated by these interesting findings on hydrogen, we investigated the dynamical properties of Ar(H$_2$)$_2$ at high-$P$ and high-$T$ in the search of similar physical manifestations and to provide further understanding of vdW compounds in general. There exist several well-established techniques by which one can determine the melting line of a material; these essentially base on solid-liquid phase coexistence simulations and/or Gibbs free-energy calculations \[23\]. Application of these methods at quantum first-principles level of description, however, turns out to be computationally very intensive and laborious. A simulation approach that has proved successful in reproducing general melting trends in materials at affordable computational cost, including experimental negative melting slopes, is the ‘heat-until-it-melts’ method \[24,25\]. This technique allows for estimation of a precise upper bound of the solid-liquid phase boundary of interest. It must be stressed that we did not pursue accurate calculation of the melting line of Ar(H$_2$)$_2$ but to identify possible anomalous effects on it.

Results from our AIMD simulations are shown in Figure 5 and can be summarized as follows: (i) the lattice of H$_2$ molecules melts at temperatures significantly lower than the whole crystal does so leading to mixtures of liquid H$_2$ and solid Ar over wide $P - T$ ranges; (ii) the fusion of the H$_2$ lattice occurs at temperatures very close to the melting line of pure hydrogen while Ar(H$_2$)$_2$ as a whole practically reproduces the melting behavior of pure Ar up to $\sim 60$ GPa; (iii) the value of the estimated $\partial T_m/\partial P$ slope is negative within the pressure interval $60 \leq P \leq 110$ GPa whereas positive elsewhere. Results (i) and (ii) can be interpreted in terms of similar arguments than recently disclosed in solid mixtures of Ne-He and Ar-He, namely: lattices composed of same-species particles effectively behave like not interacting one with another but following alike physical trends (bond distance, compressibility, etc.) than found in their respective pure system \[11\]. In fact, we recently conjectured the superior energy stability of the MgCu$_2$ structure over MgZn$_2$ in Ar(H$_2$)$_2$, as rigorously demonstrated here, using this type of reasoning and crystal symmetry arguments \[11\]. Regarding result (iii), this is in itself a manifestation of a very peculiar and intriguing physical phenomenon. In general, systems presenting negative melting slopes are characterized by open crystalline structure (water and graphite), surpassing promotion of valence electrons in the fluid phase (alkali metals) or continuous changing interparticle interactions (molecular hydrogen). In the present case either open crystalline structure or electronic band promotion effects (energetically prohibitive) can be ruled out, so changes in the interparticle interactions holds as the likely cause. The question to be answered next then is: what is the exact nature of these changing interactions?, or more precisely, do they relate to dramatic changes in electronic structure? are the ionic degrees of freedom and effective decoupling of the Ar and H$_2$ lattices crucial to them? In order to detect possible electronic phase transitions and/or molecular dissociation processes, we performed meticulous averaged DOS and H-H radial correlation function ($g_{HH}$) analysis over the atomic configurations generated in the AIMD runs. Within the thermodynamic range $60 \leq P \leq 110$ GPa and $0 \leq T \leq 3500$ K (where $\partial T_m/\partial P \leq 0$), we found that Ar(H$_2$)$_2$ is always an insulator material, either solid or liquid, where H$_2$ molecules remain stable. Therefore, dramatic changes in electronic structure can be discarded...
as the originating mechanism behind the alternating sign of $\partial T_m/\partial P$. Actually, on the contrary case, one would have expected the value of $\partial T_m/\partial P$ to be negative also beyond $\sim 110$ GPa since in principle there is no reason to think that the originating electronic effects go missing at higher-$P$. Interestingly, at compressions above $\sim 210$ GPa and temperatures high enough for the system to melt we did observe closure of the electronic energy band gap; according to $g_{\text{H-H}}$ analysis and visual recreation of the AIMD configurations, this electronic phase transition is a consequence of emergent H$_2$ dissociation processes. In Figure 6 we enclose DOS and $g_{\text{H-H}}$ results that illustrate this insulator-to-metal phase transition. It is worth noticing that this result is consistent with shock-wave compression experiments and ab initio investigations performed on pure hydrogen. With regard to the predicted negative melting slope, ionic effects are the likely subjacent cause. Considering results (i) and (ii) above, one can envisage a plausible explanation of this phenomenon: since the lattice of H$_2$ molecules melts at temperatures much lower than the lattice of Ar atoms does, collisions between diffusive H$_2$ molecules and localized Ar atoms act like effective thermal-like excitations on the last that ultimately provoke the global melting of the system at temperatures below those of pure Ar. H$_2$ itself presents negative melting slope beyond $\sim 60$ GPa so this effect is echoed, and enhanced significantly, in the melting line of Ar(H$_2$)$_2$ (see Figure 5). Beyond $\sim 110$ GPa, the stability of the Ar lattice becomes further reinforced so the effect of H$_2$ collisions there is just to deplete the slope of the global melting curve in comparison to that of pure Ar. In order to test the validity of such hypothesis, we performed a series of AIMD simulations at $P \sim 110$ GPa ($V = 7.50$ Å$^3$/particle) in which we kept the lattice of H$_2$ molecules frozen and left the lattice of Ar atoms to evolve. Under these conditions we found that fusion of the Ar structure occurs at temperatures $\sim 900$ K above that of pure Ar, hence the original melting mechanism proposed seems to be corroborated. Analogous melting behavior than described here can be expected in other rare gas-H$_2$ compounds, like Xe(H$_2$)$_7$, and maybe also in SiH$_4$(H$_2$)$_2$ and CH$_4$(H$_2$).

IV. CONCLUDING REMARKS

To summarize, we have studied the behavior of Ar(H$_2$)$_2$ under pressure at low and high temperatures using computational first-principles techniques. As results, we have unravelled (i) temperature(pressure)-induced solid-solid phase transitions that may resolve the existing discrepancies between the sets of R and IR experimental data, and (ii) an anomalous melting phenomenon consisting of negative melting slope. The atypical melting line of Ar(H$_2$)$_2$ can be understood in terms of the decoupling of H$_2$ and Ar ionic degrees of freedom and of coexistence of same-species liquid and solid phases. Metallization of liquid Ar(H$_2$)$_2$ is predicted at high $P - T$ conditions.

Acknowledgments

DE acknowledges support of MICINN of Spain (Grants No. CSD2007-00045 and MAT2007-65990-C03-01). The authors acknowledge computational resources on the U.K. National Supercomputing HECToR service.

* Electronic address: c.silva@ucl.ac.uk

1. M. Städle and R. Martin, Phys. Rev. Lett 84, 6070 (2000); P. Loubeyre, F. Occelli and R. Letoullec, Nature 416, 613 (2002)
2. C. Narayana, H. Luo, H. Orloff and A. L. Ruoff, Nature (London) 393, 46 (1998)
3. P. Loubeyre, R. Letoullec and J-P. Pinceaux, Phys. Rev. Lett. 72, 1360 (1994)
4. T. A. Strobel, M. Somayazulu and R. J. Hemley, Phys. Rev. Lett. 103, 065701 (2009)
5. E. Zurek, R. Hoffmann, N. W. Ashcroft, A. R. Oganov and A. O. Lyakhov, PNAS 106, 17640 (2009)
6. F. Daichi, P. Loubeyre, R. Letoullec, A. F. Goncharov, R. J. Hemley and H. K. Mao, Bull. Am. Phys. Soc. 41, 564 (1996)
7. S. Bernard, P. Loubeyre and G. Zérah, Europhys. Lett. 37, 477 (1997)
8. N. Matsumoto and H. Nagara, J. Phys.: Condens. Matter 19, 365237 (2007)
9. M. Somayazulu et al., Nature Chem. 2, 50 (2010)
10. H. Chacham and B. Koiller, Phys. Rev. B 52, 6147 (1995)
11. C. Cazorla, D. Errandonea and E. Sola, Phys. Rev. B 80, 064105 (2009)
12. G. Kresse and J. Furthmüller, Phys. Rev. B 54, 11169 (1996); Y. Wang and J. P. Perdew, Phys. Rev. B 44, 13298 (1991)
13. H. J. Monkhorst and J. D. Pack, Phys. Rev. B 13, 5188 (1976)
14. G. Kresse, J. Furthmüller and J. Hafner, Europhys. Lett. 32, 729 (1995)
15. D. Alfé, Comp. Phys. Comm. 180, 2622 (2009)
16. H. Fukui, N. Hirao, Y. Ohishi and A. Q. R. Baron, J. Phys.: Condens. Matter 22, 095401 (2010)
17. D. M. Ceperley and B. I. Alder, Phys. Rev. Lett. 45, 566 (1980)
18. L. Vočadlo, D. Alfé, M. J. Gillan, I. G. Wood, J. P. Brodholm and G. D. Price, Nature 424, 536 (2003)
19. L. Ulivi, R. Bini, P. Loubeyre, R. Letoullec and H. J. Jodl, Phys. Rev. B 60, 6502 (1999)
20. S. A. Bonev, E. Schwenger, T. Ogitsu and G. Galli, Nature (London) 431, 669 (2004)
21. S. Deemyad and I. Silvera, Phys. Rev. Lett. 100, 155701 (2008)
22. E. Pechenik, I. Kelson and G. Makov, Phys. Rev. B 78, 134109 (2008)
23. M. J. Gillan, D. Alfé, J. Brodholm, L. Vočadlo and G. D.
Price, Rep. Prog. Phys. 69, 2365 (2006); D. Alfè, M. J. Gillan and G. D. Price, Nature 401, 462 (1999).

24 I. Tamblyn, J-Y. Raty and S. A. Bonev, Phys. Rev. Lett. 101, 075703 (2008)

25 J-Y. Raty, E. Schwegler and S. A. Bonev, Nature 449, 448 (2007)

26 S. T. Weir, A. C. Mitchell and W. J. Nellis, Phys. Rev. Lett. 76, 1860 (1996).