Monochromatic neutrinos generated by dark matter and the see-saw mechanism

Emilian Dudas\textsuperscript{a}, Yann Mambrini\textsuperscript{b} and Keith A. Olive\textsuperscript{c}

\textsuperscript{a} CPHT, Ecole Polytechnique, 91128 Palaiseau Cedex, France
\textsuperscript{b} Laboratoire de Physique Théorique Université Paris-Sud, F-91405 Orsay, France. and
\textsuperscript{c} William I. Fine Theoretical Physics Institute, School of Physics and Astronomy, University of Minnesota, Minneapolis, MN 55455, USA

We study a minimal extension of the Standard Model where a scalar field is coupled to the right handed neutrino responsible for the see-saw mechanism for neutrino masses. In the absence of other couplings, below 8 TeV the scalar $A$ has a unique decay mode $A \to \nu\nu$, $\nu$ being the physical observed light neutrino state. Above 8 (11) TeV, the 3-body (4-body) decay modes dominate. Imposing constraints on neutrino masses $m_\nu$ from atmospheric and solar experiments implies a long lifetime for $A$, much larger than the age of the Universe, making it a natural dark matter candidate. Its lifetime can be as large as $10^{29}$ seconds, and its signature below 8 TeV would be a clear monochromatic neutrino signal, which can be observed by ANTARES or IceCube. Under certain conditions, the scalar $A$ may be viewed as a Goldstone mode of a complex scalar field whose vacuum expectation value generates the Majorana mass for $\nu_R$. In this case, we expect the dark matter scalar to have a mass $\lesssim 10$ GeV.

I. INTRODUCTION

The Standard Model (SM) of particle physics is now more than ever motivated by the recent discovery of the Higgs boson at both the ATLAS \cite{Aad:2012tfa} and CMS \cite{Chatrchyan:2012ufa} detectors. However, there are still two missing pieces in this elegant picture: the nature of dark matter (DM) and the origin of neutrino mass. Despite the fact that a window for low mass dark matter candidates (below 100 TeV) seems favored by an upper bound coming for perturbative unitarity \cite{Feng:2010gw}, no evidence has been found after many years of experimental searches \cite{Ade:2013xsa}. On the other hand, the presence of new physics at an intermediate scale seems motivated by the stability of the Higgs potential \cite{Guth:1980zm} \cite{Susskind:1984sp}, the see-saw mechanism \cite{Minkowski:1977sc} \cite{GellMann:1980vs}, leptogenesis \cite{Hannestad:2009ae} \cite{Savage:2013rja} or reheating processes. Added to the fact that a super–heavy DM, or WIMPZILLA \cite{Pospelov:2007mp} could be produced by non–thermal processes and explain the DM density in the universe, it seems natural to link the mechanism for generating a neutrino mass with the dark matter question in a coherent framework at an intermediate scale.

An intermediate scale (of order $10^{10}$ GeV) will never be reached by an accelerator on earth. The 100 TeV collider is still a state of mind project, whereas the ILC can reach, at most, a beyond the SM (BSM) scale of 100 TeV through precision measurement. However, we know that energies as large as $10^{10}$ GeV are measured in ultra-high energy cosmic rays experiments like the Auger observatory \cite{Aab:2011ad}. Recently, the IceCube collaboration claimed the detection of multi PeV ($10^6$ GeV) events \cite{Aartsen:2013bka}, giving the community some hope that an intermediate scale can be testable in the near future with these types of experiments.

In this letter we show that a high energy neutrino signal can be associated with a long-lived scalar dark matter candidate. We show that this scalar can account for the dark matter in the Universe and moreover, its specific decay mode into two monochromatic neutrino states gives a clear signature detectable in present high energy detectors like IceCube \cite{Aartsen:2013bka}. We then attempt to relate this candidate with the pseudo-Goldstone mode associated with generating the right-handed neutrino mass, necessary for the see-saw mechanism. We draw our conclusions in section V.

II. DARK MATTER AND A STANDARD SEE–SAW MECHANISM

A. The model

As a simple extension to the SM with a neutrino see-saw mechanism, we add a single real scalar field, $A$, coupled to the right handed (sterile) sector. The Lagrangian can then be written as

$$\mathcal{L} = \mathcal{L}_{\text{SM}} + \mathcal{L}_\nu + \mathcal{L}_A$$

(1)
with
\[ \mathcal{L}_\nu = -\left( \frac{1}{2} M^R + \frac{i h}{\sqrt{2}} A \right) \bar{\nu}^c_R \nu_R - \frac{y_{LR}}{\sqrt{2}} \bar{\nu}^c_L H \nu_R + h.c. \] (2)
and
\[ \mathcal{L}_A = -\frac{\mu_A^2}{2} A^2 - \frac{\lambda_A^4}{4} A^4 - \frac{\lambda_{HA}}{4} A^2 H^2 + \frac{1}{2} \partial_\mu A \partial^\mu A \] (3)
where \( H \) represents the real part of the SM Higgs field. Here, we have simply assumed that the right-handed neutrino has a Majorana mass, \( M^R \). We will explore a dynamical version of this extension in section IV.

The scalar \( A \) is massive and couples to the SM Higgs, but does not itself get a vacuum expectation value (vev). While there is no natural value for the mass scale \( M^R \), demanding gauge coupling unification in different schemes of SO(10) breaking naturally leads to intermediate scales between \( 10^6 \) and \( 10^{14} \) GeV \[14\] \[15\]. It seems then reasonable to expect that \( M^R \) will lie in this energy range if one embeds our model in a framework where one imposes unification of the gauge couplings. However, we will attempt to stay as general as possible.\[1\] In the context of very light scalar \( A \), of order a keV (though not considered in the present work), some authors have looked at the effect of a decaying \( A \) on the CMB \[17\] and more recently the subleading effect of decays to photons \[18\].

**B. The see–saw mechanism**

Once symmetry breaking is realized, the mass states in the neutrino sector are mixed in the current eigenstate basis. Diagonalization of the mass matrix leads to the well known see–saw mechanism. We can write the mass term
\[ \mathcal{L}_\nu = -\frac{1}{2} \bar{n} \mathcal{M} n, \] with \( n = \begin{pmatrix} \nu_L + \nu^c_L \\ \nu_R + \nu^c_R \end{pmatrix} = \begin{pmatrix} n_1 \\ n_2 \end{pmatrix} \]
and
\[ \mathcal{M} = \begin{pmatrix} 0 & m_D \\ m_D & M^R \end{pmatrix}, \] (4)
with \( m_D = y_{LR} v_H / \sqrt{2} \) (\( v_H = 246 \) GeV being the Higgs vev). \( \mathcal{M} \), being a complex symmetric matrix, can be diagonalized with the help of one unitary matrix \( U \), \( \mathcal{M} = U m U^T \) with
\[ m = \begin{pmatrix} m_1 & 0 \\ 0 & m_2 \end{pmatrix}. \] (5)

From the diagonalization of \( M \)
\[ m_1 = \frac{1}{2} \left[ M^R - \sqrt{(M^R)^2 + 4m_D^2} \right] \approx -\frac{m_D^2}{M^R} \approx -\frac{y_{LR}^2 v_H^2}{2M^R} \]
\[ m_2 = \frac{1}{2} \left[ M^R + \sqrt{(M^R)^2 + 4m_D^2} \right] \approx M^R \] (6)
and the eigenvectors \( N_1 \) and \( N_2 \)
\[ \begin{pmatrix} N_1 \\ N_2 \end{pmatrix} \approx \begin{pmatrix} n_1 - \theta n_2 \\ n_2 + \theta n_1 \end{pmatrix} = \begin{pmatrix} \nu_L + \nu^c_L - \theta (\nu_R + \nu^c_R) \\ \nu_R + \nu^c_R + \theta (\nu_L + \nu^c_L) \end{pmatrix} \] (7)
where \( \tan 2\theta = -2m_D / M^R \) implying \( \theta \approx \sin \theta \approx -\frac{m_D}{\sqrt{2M^R}} \). Once the Lagrangian is expressed in terms of the physical mass eigenstates, one can compute the couplings generated by the symmetry breaking and their phenomenological consequences. \( m_1 \) corresponds to the mass of the Standard Model neutrino. We will consider \( m_1 \leq 1 \) eV from cosmological constraints through the rest of the paper.\[2\]

**III. PHENOMENOLOGY**

**A. Generalities**

To study the consequences of the model, we first rewrite the Lagrangian (2) in terms of the mass eigenstates, \( N_{1,2} \).

\[ \mathcal{L}_\nu = -\frac{y_{LR}}{2\sqrt{2}} H \left( \bar{N}_1 N_2 + \bar{N}_2 N_1 \right) - \frac{y_{LR} \theta}{\sqrt{2}} H \left( \bar{N}_2 N_2 - \bar{N}_1 N_1 \right) \]
\[ -\frac{m_1}{2} \bar{N}_1 N_1 - \frac{m_2}{2} \bar{N}_2 N_2 \]
\[ -i \frac{h}{\sqrt{2}} A \left( \bar{N}_2 \gamma^5 N_2 - \theta \bar{N}_1 \gamma^5 N_2 - \theta \bar{N}_2 \gamma^5 N_1 + \theta^2 \bar{N}_1 \gamma^5 N_1 \right) \] (8)

A look at the Lagrangian (8) implies some obvious phenomenological consequences of the coupling of the scalar to the neutrino sector. First of all, the field \( N_2 \) is not stable through its decay \( N_2 \to H N_1 \) and cannot be the dark matter candidate as in the standard see-saw mechanism. Secondly, the scalar \( A \) is not stable, and its dominant decay mode for \( M_A \lesssim 8 \) TeV is \( A \to N_1 N_1 \), as \( M_{N_2} = m_2 \) is of the order of \( M^R \) and is for now assumed to be heavier than \( A \). When we include \( A \) as part of a dynamical mechanism for generating the mass \( M^R \), we will see that the mass of \( A \) may be highly suppressed relative to \( M^R \), justifying a posteriori our assumption that \( M_A < M_{N_1} \). Moreover, because the coupling of \( A \) to \( N_1 \)

---

1 We note that a similar framework has been used in [16] to stabilize the Higgs potential up to GUT scale.

2 Notice that \( N_1 \) and \( N_2 \) are Majorana like particles.

3 We neglect the flavor structure of the SM neutrino sector as it does not affect our main conclusions.
is of order of $h\theta^2$, $A$ is naturally long-lived, and can be a good dark matter candidate as we will see below. Its decay signature should be two ultra energetic monochromatic neutrinos which is a clear observable, and could be accessible to the present neutrino experiments like IceCube, ANTARES or SuperK as we will see below. Above 8 TeV, the 3-body decay mode dominates and above 11 TeV, the 4-body decay mode dominates. In this case, the signature of decay is then no longer a monochromatic signal but a neutrino-spectrum as we will see in the next section.

B. Neutrino flux

Before computing the flux of neutrinos expected on earth from the decay of the scalar $A$, let’s first check if it can be a reliable dark matter candidate, fulfilling $\tau_A > \tau_{\text{Universe}} = 10^{17}$ seconds\footnote{A recent study\cite{19} showed that taking into account the recent BICEP2 results, the real lifetime to consider should be $\gtrsim 10^{18}$ s. However, the constraints from IceCube are much stronger ($\tau_A \gtrsim 10^{28}$ seconds for $M_A$ at the PeV scale) as we will see below.}. The 2-body decay width for $A \to N_1N_1$ is given by

$$\Gamma_A^2 = \frac{10^{-38} h^2}{8\pi} \left( \frac{m_1}{1 \text{ eV}} \right)^2 \left( \frac{10^{10} \text{ GeV}}{M_R} \right)^2 M_A$$

which gives for the total width

$$\Gamma_A = \frac{10^{-38} h^2}{8\pi} \left( \frac{m_1}{1 \text{ eV}} \right)^2 \left( \frac{10^{10} \text{ GeV}}{M_R} \right)^2 M_A \times$$

$$\left[ 1 + \frac{1}{96\pi^2} \left( \frac{M_A}{v_H} \right)^2 + \frac{1}{18432\pi^3} \left( \frac{M_A}{v_H} \right)^4 \right]$$

(13)

From the expression above, we can easily compute that for $M_A \gtrsim 10^{14} h$ GeV, the 2-body, and then for $M_A \gtrsim 11$ TeV the 4-body dominate the decay process. It will be interesting then to see what kind of constraints Icecube or ANTARES can impose on the parameter space of the model\footnote{The authors want to thank the referee for having pointed out this possibility.}

The IceCube collaboration, recently released their latest analysis\cite{13} concerning the (non)observation of ultra high energetic neutrino above 3 PeV. The PeV event rate expected at a neutrino telescope of fiducial volume $\eta_E V$ and nucleon number density $n_N$ from a decaying particle of mass $M_{DM}$, mass density and width $\Gamma_{DM}$ is\cite{20}

$$\Gamma_{\text{events}} = \eta_E V \times n_N \times \sigma_N \times L_{MW} \times \frac{\rho_{DM}}{M_{DM}} \times \Gamma_{DM}$$

$$\approx 3 \times 10^{39} \eta_E \frac{\Gamma_{DM}}{M_{DM}} \text{ years}^{-1},$$

(14)

where $\sigma_N (\approx 9 \times 10^{-34} \text{cm}^2$ at 1 PeV) is the neutrino–nucleon scattering cross section, $n_N$ is the nucleon number density in the ice ($n_N \approx n_{\text{ice}} \approx 5 \times 10^{25} \text{cm}^3$), $L_{MW}$ is the rough linear dimension of our galaxy (10 kpc) and $\rho_{DM} \approx 0.39 \text{ GeV cm}^{-3}$ the milky way dark matter density (taken near the earth for the purpose of our estimate). The volume $V$ is set to be 1 km$^3$, which is roughly the size of the IceCube detector, whereas the efficiency coefficient $\eta_E$ depends on the energy of the incoming neutrino and lies in the range $10^{-2} - 0.4$\cite{22}.

The neutrino–nucleon cross section is, however, highly dependent on the scattering energy and the authors of\cite{23} obtained

$$\sigma_N = 8 \times 10^{-36} \text{cm}^2 \left( \frac{E_{\nu}}{1 \text{ GeV}} \right)^{0.363}$$

$$= 6 \times 10^{-36} \text{cm}^2 \left( \frac{M_{DM}}{1 \text{ GeV}} \right)^{0.363}$$

(15)

Implementing Eq.(15) in the expression (14), and adding an astrophysical factor $f_{\text{astro}} \approx 1$ corresponding to the uncertainty in the distribution of dark matter in the galactic halo, one can write

$$\Gamma_{\text{events}} = 1.5 \times 10^{57} \eta_E f_{\text{astro}} \frac{\Gamma_{DM}}{M_{DM}^{0.637}} \text{ years}^{-1},$$

(16)

\footnote{An earlier analysis in another context were proposed in\cite{21}}
where $\Gamma_{DM}$ and $M_{DM}$ are expressed in GeV. Noticing that there is no background from cosmological neutrino at energies above 100 TeV, one can deduce the limit set by IceCube from the non-observation of events above 3 PeV. IceCube took data during 3 years, so asking 3 events by IceCube from the non-observation of events above 100 TeV, one can deduce the limit set that there is no background from cosmological neutrino where $\Gamma_{DM}$.

SuperK [27], ANTARES [28] and IceCube [29] its mass $M$ discovery of the third event “big bird”, one can also compare a simulated NFW galactic profile $\rho_{NFW}$ for the Milky–way. Our result differs from the constraint with $f_{\text{astro}} = 1$ only by a factor of a few (2-3). Indeed, compared to an annihilating scenario, due to the lack of quadratic enhancement in the signal, the role of the (better determined) local density is more prominent. We can thus anticipate little dependence of our conclusions on the specific galactic halo used for the analysis.

IV. DARK MATTER AND A DYNAMICAL SEE-SAW

A. The model

We would now like to ask whether or not, the scalar $A$ can be incorporated into a dynamical mechanism for generating neutrino see-saw masses. Instead of the coupling of $A$ to $\nu_R$ in Eq. (2), let us couple the right handed (sterile) sector to a complex scalar field $\Phi = S e^{i\alpha/\sqrt{2}}$. We assume that $\Phi$ is responsible for the breaking of some global symmetry so that $S$ acquires a vev. Here, we would like to stay as general as possible, and show that our framework can in fact be an illustration of any extension to the SM with dynamical breaking occurring at an intermediate scale. We now rewrite the Lagrangian as

$$\mathcal{L} = \mathcal{L}_{\text{SM}} + \mathcal{L}_\nu + \mathcal{L}_\Phi$$

with

$$\mathcal{L}_\nu = -\frac{h}{\sqrt{2}} \bar{\nu}_R^c \Phi \nu_R - \frac{y_{LR}}{\sqrt{2}} \bar{\nu}_L H \nu_R + h.c.$$
and
\[
\mathcal{L}_{\Phi} = \frac{\mu_{\Phi}^2}{2} |\Phi|^2 - \frac{\lambda_{\Phi}}{4} |\Phi|^4 - \frac{\lambda_{H\Phi}}{4} |\Phi|^2 |H|^2 + \frac{1}{2} \partial_\mu \Phi \partial^\mu \Phi^*.
\] (20)

The lagrangian above has a global $U(1)$ symmetry, under which the charges of $\nu_R$, $\nu_L$ and $\Phi$ are 1, 1 and $-2$, respectively. After symmetry breaking generated by the fields $H$ and $\Phi$, one obtains in the heavy sector,
\[
\langle S \rangle = v_S = \frac{\mu_{\Phi}}{\sqrt{\lambda_{\Phi}}}; \quad S = v_S + s; \quad M_S = \sqrt{2} \mu_{\Phi},
\] (21)

and we denote by $A$, the argument of $\Phi$ after its magnitude is shifted by $v_S$. Note that our scalar field has been promoted to a Goldstone mode and is massless at tree level. The right-handed mass, $M_R$ is now given by $h v_S/\sqrt{2}$.

B. Breaking to a discrete symmetry.

If our $U(1)$ symmetry was exact (prior to $\Phi$ picking up a vev), $M_A$ would remain massless to all orders in perturbation theory. In what follows, we will assume that the $U(1)$ symmetry is broken by nonperturbative effects down to a discrete $Z_N$ symmetry. It is actually standard in string theory that all symmetries are gauged symmetries in the UV. Some of them nonlinearly realized, in the sense that under gauge transformations one axion $\theta$ has a nonlinear transformation
\[
A_\mu \rightarrow A_\mu + \partial_\mu \alpha, \quad \Phi_i \rightarrow e^{iq_i \alpha} \Phi_i, \quad \tilde{\theta} \rightarrow \tilde{\theta} + \alpha,
\] (22)

and the lagrangian contains the Stueckelberg combination of a massive vector boson
\[
\frac{M^2}{2} (A_\mu - \partial_\mu \tilde{\theta})^2.
\] (23)

Nonperturbative effects can generate operators of the form \cite{31}
\[
\frac{c_n}{M^2 v_S^2} e^{-2\pi t} (t + i \frac{e}{2})^{\sum i} \Phi_i
\] (24)

where $t$ is a field which gets a vev and where $S_{\text{inst.}} = 2\pi N(t + i \frac{e}{2\pi})$ can be interpreted as an instanton action. Nonperturbatively generated operators \cite{24} are gauge invariant, provided that $\sum q_i = N$. The gauge field $A_\mu$ which eats the axion $\tilde{\theta}$ and the field $t$ can be very heavy and decouple at low energy. At low energies therefore one gets an effective operator
\[
e^{-\langle S_{\text{inst.}} \rangle} \frac{c_n}{M^2 v_S^2} \prod_{i=1}^n \Phi_i
\] (25)

with $c$ a numerical coefficient. At low energy, even though the $U(1)$ gauge symmetry is broken, one obtains a remnant $Z_N$ symmetry. Due to its gauge origin, it satisfies anomaly cancellation conditions \cite{22}. If the original gauge symmetry was anomaly-free (which is realized if the axionic coupling to gauge gauge fields as $\theta FF$ is absent), then anomalies have to be canceled. In particular the mixed anomalies $Z_N SU(3)_C^2$, $Z_N SU(2)_L^2$ and $Z_N U(1)_Y^2$ anomalies have to vanish modulo $N$. For three generations of neutrinos, a simple candidate anomaly-free symmetry is $Z_3$. Then the lowest order nonperturbative operator breaking $U(1)$ is
\[
e^{-12\pi(t)} c M_P (\Phi^3 + \bar{\Phi}^3) = e^{-12\pi(t)} c M_P (2 S^3 - 6 S A^2).
\] (26)

This will generate a nonperturbative mass for the field $A$
\[
M_A^2 = 12 c v_S M_P e^{-12\pi(t)}.
\] (27)

For moderate values of $(t)$ this generates a large hierarchy for
\[
\frac{M_A}{M_S} \sim e^{-6\pi(t)} \sqrt{\frac{M_P}{v_S}}.
\] (28)

C. The Signal

After the symmetry breaking, the Lagrangian \cite{19} becomes
\[
\mathcal{L}_\nu = -\frac{h}{\sqrt{2}} s \bar{N}_2 N_2 + \frac{h}{\sqrt{2}} s (\bar{N}_1 N_2 + \bar{N}_2 N_1)
\]
\[
-\frac{y_{LR}}{2 \sqrt{2}} H (\bar{N}_1 N_2 + \bar{N}_2 N_1) - \frac{y_{LR}}{2 \sqrt{2}} H (\bar{N}_2 N_2 - \bar{N}_1 N_1)
\]
\[
-\frac{m_1}{2} \bar{N}_1 N_1 - \frac{m_2}{2} \bar{N}_2 N_2
\]
\[
-\frac{h}{\sqrt{2}} A (\bar{N}_2 \gamma^5 N_2 - \theta \bar{N}_1 \gamma^5 N_2 - \theta \bar{N}_2 \gamma^5 N_1 + \theta^2 N_1 \gamma^5 N_1).
\] (29)

For $M_A \lesssim 8$ TeV, the dominant decay mode is the 2-body process $A \rightarrow N_1 N_1$ and the width of the $A$ boson is now given by
\[
\Gamma_A = \frac{10^{-38}}{4\pi} \left( \frac{m_1}{1 \text{ eV}} \right)^2 \left( \frac{10^{10} \text{ GeV}}{v_S} \right)^2 M_A
\] (30)

implying
\[
\tau_A \sim 8 \times 10^{14} \left( \frac{1 \text{ eV}}{m_1} \right)^2 \left( \frac{v_S}{10^{10} \text{ GeV}} \right)^2 \left( \frac{1 \text{ GeV}}{M_A} \right)[s].
\] (31)

Since $M_R$ is now proportional to $h v_S$, the decay rate becomes independent of $h$ if we express it in terms of $v_S$ and we are forced to consider sub-PeV masses for our dark matter candidate. As one can see, for relatively light Goldstone masses of order $1$ GeV, one can obtain lifetimes in excess of the age of the Universe for $v_S > 10^{11}$.
surprising as it seems, we obtain quite reasonable values for $v_S$, compatible with GUT-like constructions.

CONCLUSION

In this work, we have shown that a dynamical model to generate majorana neutrino masses, naturally leads to the presence of a heavy quasi-stable pseudo-scalar particle that can fill the dark matter component of the Universe and whose main decay mode into two ultra-energetic neutrino is a clear signature observable by the IceCube detector. Our work is very general and can be embedded in many grand-unified scenarios where the breaking of hidden symmetries appears at an intermediate scale.

Acknowledgements. The authors would like to thank S. Pukhov and E. Bragina for very useful discussions. This work was supported by the Spanish MICINN’s Consolider-Ingenio 2010 Programme under grant MultiDark CSD2009-00064, and the contract FPA2010-17747 and the France-US PICS no. 06482. E.D. and Y.M. are grateful to the Mainz Institute for Theoretical Physics (MITP) for its hospitality and its partial support during the completion of this work. Y.M. acknowledges partial support from the European Union FP7 ITN INVISIBLES (Marie Curie Actions, PITN-GA-2011-289442) and the ERC advanced grants Higgs@LHC. E.D. acknowledges the ERC advanced grants MassTeV. The work of K.A.O. was supported in part by DOE grant de–sc0011842 at the University of Minnesota.

[1] G. Aad et al. [ATLAS Collaboration], Phys. Lett. B 716 (2012) 1 [arXiv:1207.7214 [hep-ex]].
[2] S. Chatrchyan et al. [CMS Collaboration], Phys. Lett. B 716 (2012) 30 [arXiv:1207.7235 [hep-ex]].
[3] K. Griest and M. Kamionkowski, Phys. Rev. Lett. 64 (1990) 615.
[4] D. S. Akerib et al. [LUX Collaboration], Phys. Rev. Lett. 112 (2014) 091303 [arXiv:1310.8214 [astro-ph.CO]]; E. Aprile et al. [XENON100 Collaboration], Phys. Rev. Lett. 111, no. 2, 021301 (2013); S. Archambault et al. [PICASSO Collaboration], Phys. Lett. B 711, 153 (2012); E. Behnke et al. [COUPP Collaboration], Phys. Rev. D 86, 052001 (2012); Y. D. Akimov, H. M. Arai, E. J. Barnes, V. A. Belov, A. Bewick, A. A. Burenkov, V. Chepel and A. Currie et al., Phys. Lett. B 709, 14 (2012) [arXiv:1110.4769 [astro-ph.CO]].
[5] J. Elias-Miro, J. R. Espinosa, G. F. Giudice, H. M. Lee and A. Strumia, JHEP 1206 (2012) 031 [arXiv:1203.0237 [hep-ph]]; J. Elias-Miro, J. R. Espinosa, G. F. Giudice, G. Isidori, A. Riotto and A. Strumia, Phys. Lett. B 709 (2012) 222 [arXiv:1112.3022 [hep-ph]].
[6] O. Lebedev and A. Westphal, Phys. Lett. B 719 (2013) 415 [arXiv:1210.6987 [hep-ph]]; O. Lebedev, Eur. Phys. J. C 72 (2012) 2058 [arXiv:1203.0156 [hep-ph]].
[7] P. Minkowski, Phys. Lett. B 67 (1977) 421; M. Gell-Mann, P. Ramond and R. Slansky, in Supergravity, eds. D. Freedman and P. Van Nieuwenhuizen (North Holland, Amsterdam, 1979), pp. 315-321. ISBN 044485438x; T. Yanagida, in Proceedings of the Workshop on the Unified Theory and The Baryon Number of the Universe, eds O. Sawada and S. Sugamoto. KEK79-18 (1979); R. N. Mohapatra and G. Senjanovic, Phys. Rev. Lett. 44, 912 (1980); J. Schechter and J. W. F. Valle, Phys. Rev. D 22 (1980) 2227; J. Schechter and J. W. F. Valle, Phys. Rev. D 25 (1982) 774.
[8] J. R. Ellis and O. Lebedev, Phys. Lett. B 653 (2007) 411 [arXiv:0707.3419 [hep-ph]].
[9] M. Fukugita and T. Yanagida, Phys. Lett. B 174 (1986) 45.
[10] S. Davidson and A. Ibarra, Phys. Lett. B 535 (2002) 25 [hep-ph/0202239]; E. Nardi, Y. Nir, E. Roulet and J. Racker, JHEP 0601 (2006) 164 [hep-ph/0601084]; A. Abada, S. Davidson, A. Ibarra, F. -X. Josse-Michaux, M. Losada and A. Riotto, JHEP 0609 (2006) 010 [hep-ph/0605281]; R. Barbieri, P. Creminelli, A. Strumia and N. Tetradis, Nucl. Phys. B 575 (2000) 61 [hep-ph/9911315]; M. Raidal, A. Strumia and K. Turzynski, Phys. Lett. B 609 (2005) 351 [Erratum-ibid. B...
[11] D. J. H. Chung, E. W. Kolb and A. Riotto, Phys. Rev. D 59 (1999) 023501 [hep-ph/9802238]; D. J. H. Chung, E. W. Kolb and A. Riotto, Phys. Rev. Lett. 81 (1998) 4048 [hep-ph/9805473]; D. J. H. Chung, E. W. Kolb and A. Riotto, Phys. Rev. D 60 (1999) 063504 [hep-ph/9809453].

[12] J. Abraham et al. [Pierre Auger Collaboration], Phys. Rev. Lett. 104, 091101 (2010) [arXiv:1002.0699 [astro-ph.HE]].

[13] M. G. Aartsen et al. [IceCube Collaboration], arXiv:1405.5303 [astro-ph.HE].

[14] M. Fukugita and T. Yanagida, In *Fukugita, M. (ed.), Suzuki, A. (ed.): Physics and astrophysics of neutrinos* 1-248. and Kyoto Univ. - YITP-K-1050 (93/12,rec.Feb.94) 248 p. C.

[15] Y. Mambrini, K. A. Olive, J. Quevillon and B. Zaldivar, Phys. Rev. Lett. 110 (2013) 24, 241306 [arXiv:1302.4438 [hep-ph]]; M. Kadastik, K. Kannike and M. Raidal, Phys. Rev. D 80 (2009) 085020 [Erratum-ibid. D 81 (2010) 029903] [arXiv:0907.1894 [hep-ph]]; M. Frigerio and T. Hambye, Phys. Rev. D 81 (2010) 075002 [arXiv:0912.1545 [hep-ph]].

[16] K. Kawana, arXiv:1411.2097 [hep-ph].

[17] V. Berezinsky, A. S. Joshipura and J. W. F. Valle, Phys. Rev. D 57 (1998) 147 [hep-ph/9608307]; V. Berezinsky and J. W. F. Valle, Phys. Lett. B 318 (1993) 360 [hep-ph/9309214].

[18] M. Lattanzi and J. W. F. Valle, Phys. Rev. Lett. 99 (2007) 121301 [arXiv:0705.2406 [astro-ph]]; F. Bazzocchi, M. Lattanzi, S. Riemer-Sorensen and J. W. F. Valle, JCAP 0808 (2008) 013 [arXiv:0805.2372 [astro-ph]]; J. N. Esteves, F. R. Joaquim, A. S. Joshipura, J. C. Romao, M. A. Tortola and J. W. F. Valle, Phys. Rev. D 82 (2010) 073008 [arXiv:1007.0898 [hep-ph]]; M. Lattanzi, S. Riemer-Sorensen, M. Tortola and J. W. F. Valle, Phys. Rev. D 88 (2013) 6, 063528 [arXiv:1303.4685 [astro-ph.HE]]; S. M. Boucenna, S. Morisi, Q. Shafi and J. W. F. Valle, Phys. Rev. D 90 (2014) 5, 055023 [arXiv:1404.3198 [hep-ph]]; M. Lattanzi, R. A. Lineros and M. Taoso, arXiv:1406.0004 [hep-ph].

[19] B. Audren, J. Lesgourgues, G. Mangano, P. D. Serpico and T. Tran, arXiv:1407.2418 [astro-ph.CO].

[20] B. Feldstein, A. Kusenko, S. Matsumoto and T. T. Yanagida, Phys. Rev. D 88 (2013) 1, 015004 [arXiv:1303.7320 [hep-ph]].

[21] S. Palomares-Ruiz, Phys. Lett. B 665 (2008) 50 [arXiv:0712.1937 [astro-ph]].

[22] http://indico.cern.ch/event/278032/session/13/contribution/90/material/slides/0.pdf

[23] R. Gandhi, C. Quigg, M. H. Reno and I. Sarcevic, Phys. Rev. D 58 (1998) 093009 [hep-ph/9807264].