Safe Local Exploration for Replanning in Cluttered Unknown Environments for Micro-Aerial Vehicles

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Abstract—In order to enable Micro-Aerial Vehicles (MAVs) to assist in complex, unknown, unstructured environments, they must be able to navigate with guaranteed safety, even when faced with a cluttered environment they have no prior knowledge of. While trajectory optimization-based local planners have been shown to perform well in these cases, prior work either does not address how to deal with local minima in the optimization problem, or solves it by using an optimistic global planner.

We present a conservative trajectory optimization-based local planner, coupled with a local exploration strategy that selects intermediate goals. We perform extensive simulations to show that this system performs better than the standard approach of using an optimistic global planner, and also outperforms doing a single exploration step when the local planner is stuck. The method is validated through experiments in a variety of highly cluttered environments including a dense forest. These experiments show the complete system running in real time fully onboard an MAV, mapping and replanning at 4 Hz.

I. INTRODUCTION

Micro-Aerial Vehicles (MAVs) have the potential to perform many mapping and inspection missions for search and rescue and other humanitarian operations, where it is dangerous or impractical for humans to go. Planning is a key part of any autonomous system, and online local replanning allows for fast reactions to newly observed or dynamic parts of the environment. And while local replanning has also been recently addressed in literature, most work is shown on very low-density environments, and makes optimistic assumptions about the environment (for example, that unknown space can be treated as free before observing it) [1], [2].

However, in more cluttered, unknown environments, these assumptions may lead to poor planning results. Executing these plans can also be dangerous, both for the MAV and nearby people. For example, assuming unknown space is free in forest spaces can lead to planning directly upwards into the tree canopy, this can occur as obstacles directly above an MAV are often outside the field of view of its sensors. Alternatively if a highly conservative local planner is employed, many cluttered environment will result in the system finding no feasible paths to the goal. In this work, we present a system that combines a conservative local planner with a local exploration strategy to navigate a cluttered, unknown environment such as the forest in Fig. 1.

Different local optimization methods for avoidance problems have been recently covered in literature [3], [4], [5]. However, most do not explicitly address the problem of getting stuck in local minima. This poses a special problem in unexplored or partially unexplored environments, where only locally-optimal or reactive planners will frequently fail to find a path. Other approaches use an optimistic global planner (one that considers unknown space as free) to overcome the problem of occasionally getting stuck. While this works well in low-density environments, our work aims to show that this strategy (using an optimistic RRT* [6] for goal selection) is not effective for highly-cluttered, partially unexplored environments.

Instead, we bring in concepts from the exploration literature to the area of local replanning. We compare our optimistic global planning to performing an exploration step from the exploration-gain-based “next-best-view” planner (NBVP) when the trajectory optimization planner fails to find a feasible solution [7]. We then propose our own local exploration method, which tightly couples the local planning algorithm with a strategy that selects an intermediate goal. The method maximizes both coming closer to the final goal and potential exploration gain, increasing the chances of finding a feasible path.

To solve the problem of map representations, our method...
also uses an incrementally-built, dynamically-growing Euclidean Signed Distance Field (ESDF) to compute collision costs and gradients. The ESDF is built from a Truncated Signed Distance Field (TSDF) [8], and allows us to plan in initially unknown environments with no prior knowledge of upper bounds on map size, and does not require pre-computing the object distances in batch.

We compare different parameters for our underlying local optimization method, which is an extension of our previous work [3], when the map is known a priori or initially unknown, and then compare the success rates of various intermediate goal-finding strategies in highly cluttered environments. We then demonstrate our complete system running in real-time on-board an Asctec Firefly MAV and navigating without any prior map knowledge through both an office environment and a dense forest.

The contributions of this work are as follows:

- Extension of optimization problem for continuous-time polynomial trajectory optimization.
- A system, including mapping and planning, which conservatively handles unknown space and is able to grow the map over time.
- An active local exploration strategy for overcoming local minima even in unknown environments by finding intermediate goal points.
- Simulation benchmarks and real-world experiments in various cluttered environments.

II. RELATED WORK

While a large number of methods exist for local avoidance, we will address methods in 3 categories. The first is purely reactive methods, which do not build a map of the environment but instead plan directly in the current sensor data. While these methods are very fast and computationally efficient, they do not work well in cluttered environments where avoidance maneuvers may be non-trivial, and suffer heavily from falling into local minima. The second class is map-based local avoidance methods, which use various techniques to compute feasible and locally-optimal paths through local maps built from sensor data or a priori known global maps. The last class of work we will examine here does not focus on obstacle avoidance, but instead on maximizing exploration coverage of unknown environments. While planning collision-free paths is also a requirement for any exploration strategy, the focus is on minimizing unknown space in the final map. We will draw inspiration from some of these methods to overcome the shortcomings of using optimization-based local planners.

A. Reactive Avoidance

Reactive methods focus on reacting to incoming sensor data as quickly as possible, and so act directly on obstacles in the current sensor field of view without building persistent maps.

For instance, our previous reactive work shows a method to directly convert incoming disparity maps from stereo into object segmentations, and then uses wall-following algorithm to avoid them [9]. Florence et al. directly integrates the nearest obstacle from a disparity map into a controller that is an open-loop library of motion primitives [10]. Only inexact, local state estimation is required for this approach, and they demonstrate it in both extensive simulation and real-world experiments. Lopez et al. build a KD tree of the current sensor view pointcloud, and then perform aggressive reactive avoidance from a library of fixed-velocity but variable angle motion primitives, generated from a triple-integrator model of MAV dynamics [11].

While all three methods are shown avoiding obstacles directly in front of the MAV without prior map knowledge, they are only demonstrated on much lower obstacle densities than discussed in this paper, and suffer from not being able to avoid obstacles that are not directly in the current sensor field of view.

B. Map-Based Replanning

In contrast, most replanning methods focus on navigating in a map rather than directly on sensor data.

Richter et al. presented dynamics-aware path planning for MAVs as solving an unconstrained QP through a visibility graph generated by an RRT [12], which remains a popular method for global planning [13], but is debatably too slow to replan in real-time. Our previous work [3] combines unconstrained polynomial spline optimization with gradient-based minimization of collision costs from CHOMP [14], but is prone to local minima. Usenko et al. utilize a similar concept, but use a B-spline representation instead, and use a circular buffer-based Octomap to overcome the issue of needing a fixed map size [4]. Dong et al. also use the same general problem structure as CHOMP, but represents trajectories as samples drawn from a Gaussian Process (GP) and optimize the trajectory using factor graphs and probabilistic inference [5]. While all these methods are able to avoid obstacles and replan in real time, none offer convincing ways to overcome the problem of getting stuck in a local minima and being unable to find a feasible solution.

Pivtoraiko et al. use graph search with motion primitives to replan online [2]. However, they use an optimistic local planner: unknown space is considered traversible, and while this helps escape local minima, it is fundamentally unsafe. Chen et al. plan online by building a sparse graph by inflating unoccupied corridors within an Octomap, then optimize an unconstrained QP to get a polynomial path [1]. However, they only use 2D sensing and treat unknown space as free, again leading to potentially unsafe paths in very cluttered environments.

C. Exploration

The goal of exploration literature is not only to stay safe and avoid collisions, but to maximize the amount of information about the environment. There are many different approaches, such as greedily tracking the closest unexplored frontier [15] or simulating gas-like particles throughout the
environment to find the sparsest area of dispersion to explore [16].

Rather than tracking frontiers, some methods instead aim to maximize information gain. Charrow et al. optimize this gain over a state lattice with motion primitives as connecting edges, and then improve the plan with trajectory optimization [17]. Bircher et al. instead build an RRT tree in the unexplored space, and execute a straight-line plan to the first vertex of the most promising branch of the tree, maximizing the number of unknown voxels falling into the sensor frustum [7]. Papachristos et al. extend Bircher’s method by also optimizing the intermediate paths to maximize localization quality [18]. Similarly, Davis et al. optimize paths between next-best views to maximize coverage by introducing a coverage term to their iLQG formulation [19].

Our work combines the fast online replanning capabilities of trajectory optimization-based planning with the idea of maximizing exploration gain in a future sensor field of view. This combination allows us to overcome the tendency of local planners to get stuck with local minima, while intelligently using our model of the system to find feasible solutions.

III. PROBLEM DESCRIPTION

We aim to solve the problem of an MAV attempting to reach a goal in a previously unexplored (and completely unknown) environment. The core focus being on very obstacle-dense and cluttered environments, with forest flight as a particular example. The MAV has at least one 3D imaging sensor, either RGB-D or stereo, with a finite resolution and a fixed horizontal and vertical FOV, mounted in a fixed position. We assume that the MAV is building a map of the environment from this sensor as it navigates (Section V). We design a conservative local planner, which treats unknown space as occupied and inaccessible (Section IV). The core problem we want to address is how to design a complementary goal-finding algorithm for when the local planner gets ‘stuck’ in a local minimum (Section VI). All parts of the method should be fast enough to run online and in real-time entirely on-board the MAV.

IV. LOCAL TRAJECTORY OPTIMIZATION

Our local trajectory optimization method is an extension of our previous work [3]. We represent an MAV trajectory as a high-degree polynomial spline as in Richter et al. [12], and put soft constraints (expressed in the segment time allocation) on the maximum velocity and acceleration along the trajectory, which Mellinger et al. show makes the trajectory physically feasible for a simplified dynamics model [20].

The actual optimization minimizes a compound cost, consisting of minimizing a derivative of position such as jerk or snap as in [12] and [20], combined with the collision gradient cost from Ratliff et al. [14].

We will consider a polynomial trajectory in \( K \) dimensions, with \( S \) segments, and each segment of order \( N \). Each segment has \( K \) dimensions, each of which is described by an \( N \)th order polynomial:

\[
  f_k(t) = a_0 + a_1 t + a_2 t^2 + a_3 t^3 \ldots a_N t^N
\]

with the polynomial coefficients:

\[
  p_k = \begin{bmatrix} a_0 & a_1 & a_2 & \ldots & a_N \end{bmatrix}^T.
\]

In order to avoid numerical issues with high orders of \( t \), we instead optimize over the end-derivatives of segments within the spline [12], sorted into fixed derivatives \( \mathbf{d}_F \) (such as end-constraints) and free derivatives \( \mathbf{d}_P \) (such as intermediate spline connections):

\[
  \mathbf{p} = \mathbf{A}^{-1} \mathbf{M} \begin{bmatrix} \mathbf{d}_F \\ \mathbf{d}_P \end{bmatrix}.
\]

Where \( \mathbf{A} \) is a mapping matrix from polynomial coefficients to end-derivatives, and \( \mathbf{M} \) is a reordering matrix to separate \( \mathbf{d}_F \) and \( \mathbf{d}_P \).

The final form of the optimization problem is:

\[
  \mathbf{d}_P^* = \arg\min_{\mathbf{d}_P} \left(w_d J_d + w_c J_c + w_g J_g\right)
\]

Where the derivative cost, \( J_d \), aims to minimize a certain derivative (often jerk or snap) of the position [20], with \( \mathbf{R} \) as the augmented cost matrix.

\[
  J_d = \mathbf{d}_P^T \mathbf{R}_F \mathbf{d}_F + \mathbf{d}_P^T \mathbf{R}_P \mathbf{d}_P + \mathbf{d}_P^T \mathbf{R}_S \mathbf{d}_S + \mathbf{d}_P^T \mathbf{R}_P \mathbf{d}_P
\]

The collision cost, \( J_c \), is an approximation of the line integral of costs along the path, where \( c(x) \) is the collision cost from the map, \( f(t) \) is the position along the trajectory at time \( t \), and \( v(t) \) is the velocity at time \( t \):

\[
  J_c = \sum_{t=0}^{t_m} c(f(t)) \|v(t)\| \Delta t
\]

We extend our previous work by using a soft cost for the goal, \( J_g \), similarly to [4], and the local goal finding below.

\[
  J_g = \|f(t_{end}) - \mathbf{g}\|
\]

where

\[
  f_k(t_{end}) = \mathbf{T}_{end} \mathbf{A}^{-1} \mathbf{M} \begin{bmatrix} \mathbf{d}_F^k \\ \mathbf{d}_P^k \end{bmatrix}
\]

This allows the optimization to slightly adjust the goal point to allow better trajectories, or find feasible trajectories at all. An analysis of the effect of this term on the success rate is offered in Section VII.

In general, even with the soft cost term, the initial state of the optimization problem should have the end point be free or almost free of collisions. In our system, we set a fixed planning horizon \( r_p \), which is the maximum distance from the current state that the planner is allowed to go to. However, projecting a global goal \( \mathbf{g}_g \) onto the sphere of this radius often leads to occluded end points.

In Section VII we compare two different strategies for moving this end-goal to be a feasible end point for the spline: straight-line goal finding, which backtracks along the line from the projection of \( \mathbf{g}_g \) to the start point of the
sensor data in real time. This system, called system to incrementally build maps of arbitrary size from Signed Distance Fields (TSDFs) efficiently. This allows the recently presented a way to build ESDFs from Truncated (ESDF) built from an octomap representation, we more work [3] used a fixed-size Euclidean Signed Distance Field be efficiently queried for this information. While our original of these distances, we require a map representation that can only distances to the nearest obstacles but also the gradients obstacles in front.

allowing free entry into unknown space leads to behaviors as occupied is essential to conservative local planners, as unknown voxels in this radius to occupied. Marking unknown than or equal to the maximum planning radius, and set all unknown voxels in a small clearing radius

as unoccupied. We then generate a sparse visibility graph toward the final goal, and track the first waypoint in the graph. If the first waypoint is reached, then we keep iterating through the graph until the goal point. If at any time, the local planner is again stuck, we generate a new RRT plan.

The next strategy we consider is directly from the exploration literature, the “next-best view” planner (NBVP) from Bircher et al. [7]. Their approach consists of building a rapidly-exploring random tree (RRT) with a small number of nodes in position and yaw space, and simulating the expected view frustum of the camera sensor. The approach then selects the first node to execute in the branch that leads to the highest information gain in terms of unknown voxels that would be observed. We implement this approach for comparison; however, since there is no goal-tracking component to this exploration strategy, we use the same scheme as with the random waypoint selection: one exploration waypoint, followed by trying to reach the goal, followed by another exploration waypoint.

The final strategy is our exploration strategy, combining aspects of both the exploration strategy above and goal-tracking and sensor field of view awareness, described in detail below.

A. Proposed Method

Our method uses a similar methodology to NBVP, where the potential exploration gain of future points is evaluated by projecting the camera frustum into the voxel grid. However, we adapt the method to (i) better suit the purpose of increasing the chances of the robot making it to the goal, and (ii), to function online, in real-time in a high-rate loop. The core differences are that we do not build an RRT graph, we subsample within the view frustum, and we introduce a goal-seeking reward in addition to the exploration gain.
Our method works as follows: first, we draw the global goal \( g \) with some probability \( P_g \in (0.1) \). Otherwise, we proceed to generate \( N \) random points, \( x_n \), in the unoccupied space of the TSDF, within a maximum radius \( r \) of the start point of the trajectory \( x_s \). Note, importantly, that we use the original TSDF rather than the ESDF to select these points and evaluate the frustum, as the ESDF sets nearby unknown space to occupied for planning safety purposes.

We select a yaw \( \gamma \) for each point by finding the angle of the vector from the trajectory start \( x_s \) to the sampled point \( x_n \), to approximate the real velocity-facing yaw. For each of these points, we evaluate the exploration gain of the camera frustum at that point by counting the number of unknown voxels in the TSDF. The exploration gain function \( l(x, \gamma) \) can be expressed as:

\[
l(x, \gamma) = \#\{v|v \in \text{frustum}(x, \gamma) \cap v \in \text{unknown}(v)\}
\]

In order to run in real-time, we approximate the actual exploration gain by subsampling the frustum by a certain factor, and checking only every \( s \)th voxel. We evaluate the effect of this approximation in Fig. 2 in simulation, which shows that sampling only 5\% of the samples usually leads to an estimation error of less than 1\%, and in practice runs 3 times faster than evaluating the full frustum.

Additionally, for each point we also evaluate the distance to the global goal, normalized by the maximum distance to goal \( d_g \) (to allow consistent weighting across different settings and goal distances). This normalized distance is converted to a reward, giving the total reward function \( R \) for each point \( x_n \) as:

\[
d_g = \| g - x_n \| + r \tag{11}\]

\[
R(x_n, \gamma, g) = w_v l(x, \gamma) + w_g \frac{d_g - \| g - x_n \|}{d_g} \tag{12}
\]

Fig. 2: Error in estimation of unknown voxels in the sensor frustum (as a proxy for exploration gain), by subsampling fraction (a subsampling fraction of 0.01 = 1\% of the samples are taken). As can be seen, a sampling of 5\% of the samples yields only a maximum 4\% error in the unknown voxel estimation but could lead to up to a 20\times speedup in lookup operations.

The point with the highest reward is chosen as the next intermediate goal.

A diagram showing the complete system (including mapping) is shown in Fig. 3.

VII. SIMULATION EXPERIMENTS

This section will evaluate different aspects of our system in a simulation environment where the ground truth map is known. We compare the effects of full map knowledge vs. planning in an initially unknown map, evaluate the effect of parameters on success rate of local trajectory optimization, compare the intermediate goal finding methods presented in Section VI and the effect of subsampling the camera view frustum for exploration gain evaluation.

These simulations are made with the \textit{voxblox}, which allows generating ground-truth ESDFs for environments made of primitive shapes (in this case, cylinders to simulate trees in a forest), and also allows simulating sensor measurements by raycasting into the map. The maps are 15 meters \( \times \) 10 meters, and have an obstacle region of 10\times10, to ensure that the start and end poses are always free. Cylinders of radii between 0.1 and 0.5 and various heights are placed randomly within the space.

For the purposes of these experiments, we assume our MAV can track the polynomial trajectories perfectly, which [20] shows is possible as long as we respect maximum velocity and acceleration bounds while planning. We add a new viewpoint into the incrementally-built map and then replan once a second of simulation time. The incremental planning methods have a maximum planning horizon of 3 meters.

First, we compare multiple methods when given complete ground-truth knowledge of the map, in the low obstacle density scenario shown in Fig. 4(a) where the MAV is attempting to plan from one side of the map to the other. Intermediate paths are shown in colors, while the black line is the final executed trajectory. Fig. 5(a) shows the quantitative results: “one-shot” is a single plan using the planner described in Section IV directly from the start to the goal. This has a much higher success rate than the other planning methods, as it is able to make intelligent
decisions about which path to take around obstacles, while the incremental methods may commit to a locally optimal path and become stuck in a minimum which will not lead to the goal.

The next results are for starting with an a completely empty map, and inserting new viewpoints along the path at 1 Hz, with a sample solution shown in Fig. 4(b) and the quantitative results in Fig. 5(b). The maximum success rate for all methods is less than in the full map knowledge case in Fig. 5(a) as the local minimum problem is worse with an unknown map: there may be a path from the current state to the goal, but if it is occluded in the sensors then there is no way for the planner to find it. Additionally, increasing the number of replans or adjusting planner parameters does not substantially increase the success rate in this case, as it is a

To overcome these issues, we benchmark the intermediate goal-finding methods, described in Section VI, on the same simulation cases. Fig. 6 shows the quantitative results: as can be seen, all goal-finding methods outperform the naive optimization-only method. The optimistic RRT* performs the worst, as it tends to select the same infeasible path over and over again as unknown space is marked as traversable for this method. NBVP performs somewhat better, and we benchmark two variants: “no yaw”, which uses the velocity-tracking yaw of other methods, and “yaw”, which linearly interpolates between current yaw and the sampled yaw from NBVP. As can be seen, “no yaw” performs better in more cluttered cases as the MAV is facing the direction of travel, making it more likely to observe the areas it must traverse to be able to plan in them.

Finally, our method performs on par with random goal selection in terms of success rate. However, our method is able to consistently produce much shorter path lengths: Fig. 7 shows the mean path lengths for simulation cases that both random goal finding and our method were able to solve. Our method produces paths up to 35% shorter. It is also interesting to compare 5(a) and 6 as the incremental goal finding is able to perform better than optimization-only methods even when they are given full map knowledge.

The final experiment is a more realistic test of a long forest traversal. We generate a 50 meter × 50 meter randomized map with 0.1 obstacles/m², and set the MAV to explore from one corner to the other. The results are shown in Fig. 8 where our method was the only one successfully able to find the goal. The final path lengths and distances from goal are shown in Table I and the timings of different aspects of the method from this simulation are shown in Table II.
Fig. 7: Path length comparison between random goal selection and our proposed method. The path lengths are only evaluated for trials where both planners succeeded, to allow a fair comparison. Note that our method always finds a solution in a significantly shorter path length, as it exploits current knowledge of the environment.

![Solution Path Lengths](image)

| Method                | Distance Traveled [m] | Distance from Goal [m] |
|-----------------------|-----------------------|------------------------|
| No Intermediate Goals | 19.4                  | 51.8                   |
| Random Goals          | 206.8                 | 0.0                    |
| Optimistic RRT        | 37.4                  | 35.4                   |
| NBVP                  | 316.5                 | 42.4                   |
| Our Method            | 117.3                 | 0.0                    |

TABLE I: Long forest simulation results, where only our method and random restarts were able to find a solution, but our method is able to do so in a shorter path length.

VIII. REAL-WORLD EXPERIMENTS

To evaluate our system in a real-world scenario, we performed multiple experiments in two different test environments: a cluttered office space and a dense forest with a variable ground height. The results of all described experiments are available in the attached video.

All of the experiments start with a completely unknown map, use visual-inertial odometry from the forward-facing (with a 12° downward pitch) stereo camera, update the map from stereo and replan at 4 Hz, and run everything entirely on the 2.4 GHz i7 dual-core CPU on-board the robot.

In the office space environment, the MAV is able to navigate from a starting position in a hallway, around a corner, and to a point above an office table, shown in Fig. 9. During the path, it successfully avoids an ajar cabinet door (which blows open during the flight), along with many obstacles on either side of the hallway. The MAV is not able to reach its intended goal, as it is unable to successfully determine whether the air-space above the tables is clear or not: the tables are gray and textureless, and the white projector screen behind them is also textureless, leading to a lack of stereo matches and therefore unknown space in the map. This demonstrates the conservative and safe nature of our planner.

Our second experimental validation was performed in a forest environment, where we performed four different experiments. In the first trial, we were successfully able to avoid a single large tree between the start point and goal. Second, we did two experiments where the MAV was commanded to go a large distance in its current facing direction, where the robot successfully avoided tree branches along its way and navigated largely along a hiking trail for up to 45.0 meters. In the shorter experiment, the MAV was able to reach its goal. In the longer one, it was unable to reach the final goal as the slope of the ground was too high and the tilted-down camera did not allow it to perceive enough open space to safely raise its flying height above the ground. The final forest experiment tested navigation in very cluttered, obstacle-dense environments. The MAV was com-

![Experimental results from the office navigation experiment, with final map and intermediate paths shown on the lower right.](image)
TABLE II: Timings for each part of the method, from the benchmark in Fig. 8. Note that intermediate goal selection will only run if trajectory optimization fails.

| Step                      | Time [ms] |
|---------------------------|-----------|
| Mapping                   |           |
| TSDF Insert               | 27.0      |
| ESDF Update               | 14.5      |
| Local Replanning          |           |
| Trajectory Optimization   | 19.3      |
| Intermediate Goal Selection | 5.9    |

IX. CONCLUSIONS

This paper presented a complete system for local obstacle avoidance, consisting of an underlying trajectory optimization method, which uses an Euclidean Signed Distance Field (ESDF) built by voxblox to get collision costs and gradients, coupled with an exploration-inspired intermediate goal finding strategy to escape local minima in the optimization. We showed that our combined method outperforms the common strategy of coupling an optimistic global planner with a conservative local planner. In the case of high obstacle densities, our exploration-based method is able to find solutions to more planning problems. We also outperform the next-best view exploration method for intermediate goal, as we are able to incorporate information about the global goal and reduce the runtime of the exploration gain evaluation.

Our approach focuses on solving the case of very cluttered environments in previously unknown maps, and maximizing the chances of finding the goal while building the map. To demonstrate the performance of our method in real-world scenarios, we were able to successfully navigate through an office and through multiple forest environments while performing all processing in real-time on-board an MAV.

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