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Westig, Marc; Thierschmann, Holger; Katan, Allard; Finkel, Matvey; Klapwijk, Teun

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Marc Westig, Holger Thierschmann, Allard Katan, Matvey Finkel, and Teun M. Klapwijk

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Analysis of a single-mode waveguide at sub-terahertz frequencies as a communication channel

Marc Westig, Holger Thierschmann, Allard Katan, Matvey Finkel, and Teun M. Klapwijk

AFFILIATIONS
1 Kavli Institute of NanoScience, Delft University of Technology, Lorentzweg 1, 2628 CJ Delft, The Netherlands
2 Fachbereich Physik, Freie Universität Berlin, Arnimallee 14, 14195 Berlin, Germany

ABSTRACT
We study experimentally the transmission of an electromagnetic waveguide in the frequency range from 160 to 300 GHz. Photo-mixing is used to excite and detect the fundamental TE$_{10}$ mode in a rectangular waveguide with two orders-of-magnitude lower impedance. The large impedance mismatch leads to a strong frequency dependence of the transmission, which we measure with a high-dynamic range of up to 80 dB and with high frequency-resolution. The modified transmission function is directly related to the information rate of the waveguide, which we estimate to be about 1 bit per photon. We suggest that the results are applicable to a Josephson junction employed as a single-photon source and coupled to a superconducting waveguide to achieve a simple on-demand narrow-bandwidth free-space number-state quantum channel.

I. INTRODUCTION
An important problem in communication technology is the transmission of a coded message, from an initial point via a channel to a final point, with minimal error in receiving and decoding the message. Electro-magnetic transmission lines, such as an optical fiber or a waveguide, are attractive as a communication channel because compared to free space, they minimize the radiative information loss. The effectiveness of a channel, in terms of the information rate, is quantified by the channel capacity, measured in bits per second or in bits per photon. The most effective way of using a waveguide is by implementing a "one quantum-one bit-one mode" strategy as introduced by Caves and Drummond. Here, we analyze experimental results on the transmission of a waveguide at subterahertz (THz) frequencies in the context of this information communication-effectiveness.

Three-dimensional (3D) waveguides and cavities have recently entered the field of quantum-information technology in the form of superconducting cavities, which show at the frequencies around 10 GHz the lowest (dissipative) loss to date and, therefore, support a superior qubit operation. The reason for the low loss is the minimal relative energy stored in surface defects in 3D cavities, compared to other technologies such as planar (2D) resonators or conductors. For a 3D cavity, the relative energy loss in surface defects scales inversely proportional to its size, which is also dependent on the propagating mode because of the mode-dependent current distribution at the cavity walls. This type of technology has been developed many years ago in the field of astronomical detectors for applications at significantly higher frequencies. Developed for the astronomically important range of hundreds of gigahertz and for other sophisticated 3D submillimeter waveguide circuits, the technology appears suitable for use in quantum networks as well.

In the previous work, isotropic dispersion relations have been included in the description of the communication channel. In this case, the signal group velocity along the channel at frequency $f$ scales with all spatial dimensions along the channel, as noted by Caves and Drummond, and hence, the information rate is not modified by this isotropic dispersion. In the present work, we identify that the frequency-dependent transmission of a single-mode rectangular
waveguide carries directly over to the channel capacity. We quantify this by analytic expressions and numerical modeling. It shows that it is caused by the high-impedance source and detector, coupled to the two orders-of-magnitude lower impedance of the fundamental TE\(_{10}\) mode of the waveguide [using a waveguide of length \(l = 39.6\) (79.2) mm, i.e., which is 33 (66)-times longer than the center wavelength]. As a result, for a single frequency-multiplexed coherent-state channel, the information rate varies up to a factor of about 2 over the transmission bandwidth of 210–300 GHz.

Furthermore, in view of the recent achievements of Josephson photonics and quantum microwave radiation, we identify that a Josephson-junction based single-photon source can reliably be coupled to a single-mode waveguide using established microwave engineering techniques. If such a waveguide is coated with a superconductor and operated at low-enough temperatures, at frequencies below the gap energy of the superconductor, a Josephson-junction based on-demand number-state quantum channel can be realized. When additionally coupled to free-space, as shown in this work for a coherent state, this would also provide a feasible way to radiate a well-controlled quantum state into free space.

This paper is organized as follows: Section II describes our experimental method and setup. In Secs. III A and III B, the electromagnetic modeling results of the diagonal horn antennas and the waveguides of our setup are provided. In a second step, we connect the modeling results to the optical properties of the used photo-mixers (Sec. III C), i.e., their characteristic wave impedance, using the ABCD-matrix formalism to obtain a complete model. The measured response is presented and analyzed in Sec. IV. In Sec. V, we summarize theoretical expressions for the channel capacity in which the effect of the frequency-dependent transmission through our diagonal-horn antenna/waveguide assembly on the information rate becomes clear. It includes essential details of the capacity for two types of communication channels, a coherent-state channel and a number-state channel. Section VI discusses experimentally realized Josephson circuits which together with superconducting waveguides are well suited for implementing in free-space the concepts discussed theoretically in Sec. V. We conclude our work in Sec. VII.

II. EXPERIMENTAL SETUP

In Fig. 1, we show a sketch of a standard open rectangular waveguide and the standard prediction for the transmission using the analytical theory presented in the work of Bayer.\(^\text{10}\) Our aim is to evaluate experimentally this prediction for the subterahertz frequency range. The shown predictions are for a lossless and impedance-matched waveguide, the step-function, and two impedance-matched waveguides of different lengths including the loss in the material. A longer waveguide naturally has a lower transmissivity because of the loss of the signal occurring over the length of the waveguide. An experimental test of this prediction is currently possible because of the availability of high quality waveguides and continuously tunable sources. The full experimental setup is shown in Fig. 2(a). The central element is the waveguide, as schematically shown in Fig. 1(a) and represented in detail in Fig. 2(d). A free space subterahertz electromagnetic wave enters a diagonal horn, travels through the waveguide, and is radiated out again from a diagonal horn. The horns and waveguide are made of the same material, CuTe, using present-day computer-controlled machining technology. The frequency-tunable electromagnetic signal, in the appropriate frequency range of 160–300 GHz, is generated and detected by superimposing the outputs of two 780 nm distributed feedback (DFB) lasers in a beam combiner (BC) and illuminating two GaAs photo-mixers connected at the output of the beam combiner via polarization maintaining fibers (PMF), with one photo-mixer acting as a coherent terahertz source (S) and the second one as a coherent terahertz detector (D).\(^\text{11}\) The incident laser power on each photo-mixer is approximately 30 mW. The desired frequency of the

![FIG. 1](image-url)
terahertz electromagnetic signal is set by adjusting the difference frequency between the two DFB lasers. Optimal coupling between all optical elements is achieved by arranging the setup according to the distances summarized in Sec. III C.

Each photo-mixer consists of a metallic two-electrode log-spiral circuit, patterned on a GaAs chip. The nonpatterned side of the GaAs chip is glued on a silicon lens, employed for Gaussian beam formation. The laser spot from the optical fiber is focused on the feedpoint of the log-spiral circuit. The relevant equivalent circuits are shown in Figs. 2(b) and 2(c). The source photo-mixer is biased by a 39.6 kHz modulated on/off voltage of \( V \). The source laser is frequency locked to the subterahertz signal, tuned by the laser power. For the electromagnetic description of the photoconductive switch of the source and the detector, the characteristic wave impedance is much higher and amounts to \( R_{\text{ph}} \sim 140 \, \text{k}\Omega \). It is estimated over the generated power in the frequency range used and the resulting current flow upon detection.\(^{14} \)

We analyze the emitted terahertz field from the diagonal horn as follows: The terahertz electric field component received by the detector leads to an ac-voltage drop across an interdigitated capacitor of the detector with a frequency equal to the laser detuning \( f \). Together with the laser-induced impedance modulation with the same frequency, but in general with a different phase, a coherent \( \text{dc} \)–photocurrent, \( I_{\text{dc}}(f) \), flows in the positive or negative direction (dependent on the phase) across the feedpoint of the log-spiral circuit. The \( \text{dc} \)– photocurrent induces a voltage drop across the detection impedance \( R_{\text{ph}} \) [Fig. 2(c)], which is amplified while preserving its sign in a transimpedance amplifier (type PDA-S) with a bandwidth of 0–1 MHz. Each data-point is then integrated over 500 ms. This detection scheme resembles a homodyne detector at terahertz frequencies with a high-dynamic range up to 80 dB,\(^{14} \) as described by Roggenbuck \textit{et al.} A benefit of this scheme is that it measures the transmitted amplitude rather than only the transmitted power. In this work, we use only the instantaneous amplitude (envelope function \( \propto \sqrt{P} \)) of the Hilbert transformation of \( I_{\text{dc}}(f) \), Eq. (1), for comparison with our theoretical model,

\[
I_{\text{dc}}(f) = I_{\text{dc}}(f) + i \mathcal{H}[I_{\text{dc}}(f)] = S(f) \exp[i\phi(f)].
\]

Here, \( \mathcal{H}(\cdots) \) is the Hilbert transformation,\(^{16} \) \( \phi(f) \) is the instantaneous phase of the signal, and \( S(f) \) is the instantaneous amplitude which we show in Figs. 5 and 6 as experimental data.

Since the interplay between generation and detection of the subterahertz signal plays a crucial role in our work, we address both in a bit more detail. At the feedpoint of the log-spiral antenna, the two electrodes are coupled to a few micrometer size metal-semiconductor-metal (MSM) interdigitated capacitor, having a square geometry. It functions as a photoconductive switch, since the GaAs chip becomes slightly conducting in the region of the interdigitated capacitor when charge carriers are created by the laser light, followed by recombination with the emission of phonons, characterized by a measured time scale of \( \tau_c = 500 \, \text{fs} \). The interdigitated capacitor fingers are about 1 \( \mu \text{m} \) apart. The \( \text{dc} \)-resistance of the photoconductive switch is typically of the order of \( R_{\text{ph}} \sim 10–30 \, \text{k}\Omega \) when the switch is closed, dependent on the charge carrier density, tuned by the laser power. For the electromagnetic description of the photoconductive switch of the source and the detector, the characteristic wave impedance is much higher and amounts to \( R_{\text{ph}} \sim 140 \, \text{k}\Omega \). It is estimated over the generated power in the frequency range used and the resulting current flow upon detection.\(^{17} \)

We assume that the characteristic impedance contains no reactive components, which appears adequate to describe our experimental results.

The initially uncorrelated laser fields are coupled by the nonlinear, i.e., quadratic, dependence of the charge carrier creation in...
GaAs (causing the frequency mixing). Detuning the DFB lasers by the frequency \( f \), the impedance of the MSM interdigitated capacitor is modulated by the same frequency. In other words, the switch is opened and closed on a time scale \( \sim (2\pi f)^{-1} \gg (2\pi f_c)^{-1} \), which in our frequency range is much slower than the characteristic time scale \( (2\pi f_c)^{-1} = \tau \) of the recombining carriers in GaAs. Furthermore, the antenna impedance of the log-spiral circuit, \( R_{\text{ant}} = 72 \ \Omega \), together with the photo-mixer capacitance \( C \), defines an RC-time, which in our used frequency range is much shorter than the time period of the generated waves due to the frequency mixing, \( RC \ll (2\pi f)^{-1} \).

Hence, together with the application of the dc-bias voltage, a terahertz current with frequency \( f \) oscillates in the MSM interdigitated capacitor and excites the log-spiral circuit. The log-spiral circuit has a counter-clockwise direction of turn in the propagation direction of the beam. Due to this geometry, it emits a left-circular polarized terahertz field through the silicon lens, indicated by the dashed red circle in Figs. 2(a) and 2(b). Sending the left-circular polarized terahertz field through the diagonal-horn antennas and the rectangular waveguide, as shown in Figs. 2(a) and 2(d), the output field is linear polarized [the red linear arrow at the output of the waveguide in Fig. 2(a)]. The reason for this is the confined parallel-plate-like geometry of the rectangular waveguide, as shown in Figs. 2(a) and 2(d). In Fig. 2(d), the cut through the full-height rectangular waveguide indicates the hollow region with area \( 2b^2 \) machined in the CuTe material. For the fundamental TE_{11} mode, this geometry only supports field lines perpendicular to the a-side and parallel to the b-side; hence, an electromagnetic field with a linear polarization is characteristic for this waveguide mode. Due to the conversion from a circular-polarized to a linear polarized mode in the waveguide, the output power is lowered by a factor of 2. It is further decreased by additional, albeit small, waveguide losses when considering that the traveling distance through the waveguides with lengths \( l = 39.6 \ \text{mm} \) and \( l = 79.2 \ \text{mm} \) corresponds to many wavelengths \( (\lambda \sim 1.2 \ \text{mm}) \) in our frequency range.

The detector is operated without applying a bias voltage to it, and it is pumped by the same two DFB lasers through the beam combiner, such as the source. This again modulates the impedance of the MSM interdigitated capacitor at the frequency \( f \), but this time in the detector. The impinging terahertz electromagnetic field on the detector is received by its log-spiral circuit and is characterized by an amplitude and phase which we obtain by postprocessing using a Hilbert transformation of the real-valued detector photocurrent \( I_d(f) \), Eq. (1).

### III. ELECTROMAGNETIC MODELING AND QUASIOPTICAL PROPERTIES

The measured data will be compared with model-data in Fig. 6. Therefore, we first describe the electromagnetic model which captures the full system. It is built from a separate analysis of the diagonal horn antennas (Sec. III A) and the rectangular waveguide (Sec. III B). These separate parts are then combined to a full model of the assembled device, including the coupling to the source and the detector (Sec. III C). We use the standard ABCD-matrix formalism to obtain for each frequency the scattering parameter which subsequently can be compared to the measured transmission; cf. Fig. 6. The details of this approach are given below.

#### A. Diagonal-horn antenna

A three-dimensional finite element simulation of the diagonal-horn antennas has been conducted based on the CST software.\(^\text{19}\) The optimization of the antenna performance is achieved by varying the inner-conductor shape and length in the simulation. To obtain a compact device and to minimize the dissipative loss, a short antenna is favored, provided it still has a low enough return loss and reasonable quasioptical beam properties. In the CST model, the antenna design is built upon mesh cells, with the metallic boundary conditions imposed to define the electromagnetic properties. The feedpoint (cf. Fig. 4, upper panel) has been implemented with an ideal impedance-matched waveguide port to minimize parasitic reflections. The waveguide port is also used as the excitation source for the simulation. The output (or the input, where the antenna is employed as a receiving device) of the diagonal-horn antenna is terminated by the free space impedance \( Z_\infty = \mu_0 \epsilon_0 c \), with \( \mu_0 \) being the vacuum permeability and \( \epsilon_0 \) being the velocity of light in vacuum. A Vivaldi shape with a smooth transition to straight edges at the output, cf. the upper panel of Fig. 4, yields a minimum input reflection \( S_{11}(f) \) over the broad range of frequencies used in the experiment.

As a final step, we have included the designed antenna geometry in a three-dimensional construction model prepared in Autodesk Inventor.\(^\text{20,21}\) Through this, we achieve a one-to-one correspondence between the anticipated optical properties in the simulated diagonal horn antennas and the optical properties of the fabricated diagonal-horn antennas.

Our simulation results are summarized in Fig. 3. In the main figure, we show the input impedance \( Z(f) \), and the inset shows \( S_{11}(f) \) as a black solid line. Both quantities are referred to the feedpoint. Note the waviness of \( Z(f) \) of the diagonal-horn antenna, which indicates a less than perfect match to the free-space impedance. The waviness can be reduced at the cost of a longer antenna with a smoother transition from the feedpoint waveguide to its output. As an illustration, we compare in the same figure the input impedance of the diagonal-horn antenna and the one of an input-matched rectangular full-height waveguide with the same dimensions as the antenna feedpoint. Obviously, they follow the same trend, but the impedance function of the waveguide is smooth. These simulations take into account the conductor loss \( \alpha_c \) of the diagonal horn and waveguide material CuTe (the inset of Fig. 1).

We include the expected dissipative loss in the simulation for the diagonal-horn antennas although it is known to be rather low in this antenna type. The reason is the advantageous field distribution,\(^\text{22}\) which drives surface currents parallel to the mechanical cut shown in Fig. 4. The calculated realized gain and the directivity in the antenna simulation are used to determine the antenna efficiency. From this, a dissipative loss in the antenna of \( -0.53 \ \text{dB} \) in the center of the frequency band is found, small enough to approximate a reciprocal network. This approximation facilitates subsequent modeling. The input-reflection scattering parameter, \( S_{11}(f) \), and the scattering parameter from the feedpoint to the antenna output, \( S_{31}(f) \), can be expressed as
A convenient way to achieve this is to exploit the ABCD-matrix formalism. In the case of a receiving diagonal-horn antenna, we combine in Sec. III C the scattering parameter pair derived from the ABCD-matrix formalism is shown for comparison as long-dashed lines. The waveness in the result for the diagonal-horn antenna compared to the ideal waveguide result shows the expected imperfection for our system when matching a rectangular waveguide via our diagonal-horn antenna to free space. The inset shows the simulated input reflection scattering parameter \( S_{11} \) and the resultant (calculated) scattering parameter \( S_{21} \) from the antenna feedpoint to its output as black solid and red short-dashed lines. The corresponding scattering-parameter pair derived from the ABCD-matrix formalism is shown for comparison as long-dashed lines.

\[
\begin{align*}
S_{11}(f) &= |S_{11}(f)| \exp[i\theta(f)] , \\
S_{21}(f) &= \sqrt{1 - |S_{11}(f)|^2} \exp[i\phi(f)] .
\end{align*}
\]

In the equations, \( \theta(f) = \arctan(\text{Im}[S_{11}(f)]/\text{Re}[S_{11}(f)]) \) is the argument of the complex-valued function \( S_{11}(f) \) and \( \phi(f) = \theta(f) + \pi/2 \). Due to the reciprocal-network approximation, Eqs. (2) describe the antenna as an emitting as well as a receiving device, \( S_{12} \approx S_{11} \). For the back-to-back configuration shown in Fig. 1(a), \( S_{12} \) is the scattering parameter from the input to the antenna feedpoint for the receiving antenna, which connects to the waveguide. This means in particular that deriving \( S_{11} \) as a function of frequency is sufficient to determine the full set of scattering parameters for the diagonal-horn antenna.

Since the diagonal-horn antenna and waveguide device consist of three elements, a receiving diagonal-horn antenna, a rectangular full-height waveguide of length \( l \), and an emitting and identical output diagonal-horn antenna, we combine in Sec. III C the electromagnetic properties of the three elements into a full model. A convenient way to achieve this is to exploit the ABCD-matrix formalism, which permits the combination of an arbitrary number of (two-port) microwave elements to calculate the full set of scattering parameters for the complete microwave element assembly. The transformation between ABCD- and S-parameters for a two-port network with complex termination impedances is given by the matrix elements

\[
\begin{align*}
A &= \frac{(Z_{01}^* + S_{11}Z_{01})(1 - S_{22}) + S_{12}S_{21}Z_{01}}{2S_{21}\sqrt{R_{02}R_{02}}} , \\
B &= \frac{(Z_{01}^* + S_{11}Z_{01})(Z_{02}^* + S_{22}Z_{02}) - S_{12}S_{21}Z_{01}Z_{02}}{2S_{21}\sqrt{R_{02}R_{02}}} , \\
C &= \frac{(1 - S_{11})(1 - S_{22}) - S_{12}S_{21}}{2S_{21}\sqrt{R_{02}R_{02}}} , \\
D &= \frac{(1 - S_{11})(Z_{02}^* + S_{22}Z_{02}) + S_{12}S_{21}Z_{02}}{2S_{21}\sqrt{R_{02}R_{02}}} \\
\end{align*}
\]

and

\[
\begin{align*}
S_{11} &= A Z_{02} + B - C Z_{01}^* Z_{02} - D Z_{01}^* , \\
S_{12} &= 2(AZ_{02} + B + CZ_{01}Z_{02} + DZ_{01}) , \\
S_{21} &= AZ_{02} + B + C Z_{01}^* Z_{02} + DZ_{01} , \\
S_{22} &= -AZ_{02}^* + B - C Z_{01} + DZ_{01} .
\end{align*}
\]
In general, in the equations above, every parameter is also a function of frequency, which we include in our modeling. In addition, $Z_{01}$ and $Z_{02}$ are the complex termination impedances. The * symbol indicates the complex conjugate, and $R_{01}$ and $R_{02}$ are the real parts of the complex termination impedances.

By applying Eqs. (3), we find the frequency dependent ABCD-parameters of the diagonal-horn antenna from the previously determined set of S-parameters. In this calculation, $Z_{02} = Z_{\infty}$ is the free space impedance terminating the diagonal-horn antenna and $Z_{01} = (\omega/c_0)Z_{\infty}/\beta$, with $\omega$ being the angular frequency and $\beta$ being the feedpoint waveguide complex propagation constant. We first use the nominal dimensions of the antenna’s feedpoint waveguide to evaluate $\beta = \sqrt{(\omega/c_0)^2 - (\pi/a)^2}$, where $a = 2b = 800$ $\mu$m. By back-transformation to the S-parameters using Eqs. (4), we evaluate the precision of this procedure in the inset of Fig. 3 (long-dashed lines) with the previously simulated $S_{11}$-parameter and calculated $S_{11}$-parameter (solid and short-dashed lines). In general, we find a satisfactory agreement for all frequencies, and the agreement is better for increasing frequency. At the lowest frequencies, the deviation amounts to at most 8%, accurate enough to permit a comparison to our experimental results.

**B. Rectangular waveguide**

The standard ABCD-parameters for the rectangular waveguide are

$$
A_{wg} = \cosh (y l), \quad B_{wg} = Z_{01} \sinh (y l), \quad C_{wg} = Z_{01}^{-1} \sinh (y l), \quad D_{wg} = \cosh (y l).
$$

(5)

They take the same form as for the usual transverse-electromagnetic (TEM) transmission line, such as a coaxial cable. The only difference is the value of the complex propagation constant $\gamma$, due to the cutoff in the frequency spectrum of $\beta$ and its frequency dependence. $\gamma = \alpha_c + i\beta$, with $\alpha_c$ and $\beta$ as discussed above.

**C. Complete setup and quasi-optics**

Multiplying the ABCD-matrices of the single elements in the order as they appear in the setup shown in Fig. 1(a), i.e., receiving diagonal-horn antenna, rectangular waveguide of length $l$, and emitting diagonal-horn antenna, one obtains the full ABCD-matrix of the setup. Using the relations in Eqs. (4) for the $S$-parameters, with $R_{1CD} = Z_{0102} = 140$ k$\Omega$ (Sec. II) as the real-valued source and detection characteristic wave impedances, one obtains the total S-parameter set of the experimental setup, which should be proportional to the transmission we measure in the experiment.

Finally, we introduce the experimentally relevant Gaussian, i.e., quasi-optical, beam properties of the source/detector and the diagonal-horn antenna, which is important in optimizing the experimental setup. First, the Gaussian beam profiles of the source and detector are slightly asymmetric in their $xz$- and $yz$-planes, with $z$ being the propagation direction of the field shown in Fig. 1(a). This is quantified by the beam waist radii in these planes, $w_{xz} \sim 2$ mm and $w_{yz} \sim 2.2$ mm, which are located at distances $\sim 25$ mm and $\sim 32$ mm from the aperture. The optical properties of the diagonal-horn antenna, although having slightly curved instead of linear slanted walls, are best approximated by the analytical theory by Johansson and Whyborn. From their theory, we obtain for our diagonal-horn antenna design a waist radius of $w_{xz} = w_{yz} = 1.9$ mm, a distance of $z_A = 14$ mm between the position of the beam waist and the aperture, and a Rayleigh length of $l_c = 9.6$ mm. Additionally, the beam curvature at the aperture is characterized by the radius $R_A = 20.6$ mm and the beam waist at the aperture is $w_A = 1.77 w_0$. For maximum optical coupling, we arranged the photo-mixers and the diagonal-horn antennas such that the respective beam waists were on top of each other. Optimizing the position of the photo-mixers with respect to the diagonal-horn antennas has been achieved by moving them with micrometer precision in order to maximize the photocurrent and to compensate for their aforementioned beam asymmetry.

**IV. EXPERIMENTAL RESULTS AND ANALYSIS**

The full results from the measurements and the model analysis for three different waveguides are shown in Fig. 6. Panel (a) (79.2 mm waveguide, experiment) and panel (b) (79.2 mm waveguide, model) are the transmission (proportional to $S_{21}$) as a function of frequency. Panels (c) and (d) show the results for the two short waveguides (39.6 mm), with panel (c) showing the experiment and panel (d) the model. Obviously, all three waveguides become transmissive around 210 GHz [panels (a) and (c)], the anticipated by design waveguide cutoff. In addition, it is also clear that the two short waveguides show a very similar pattern as a function of frequency and short-period oscillations as a function of frequency. Third, we also observe that the twice longer waveguide, panel (a), shows more variation in the transmissivity as a function of frequency than the two shorter ones. These variations occur on a much longer frequency scale than the features observed in the two shorter waveguides. To proceed toward a quantitative evaluation, which in the end will provide the communication rate of the waveguide, we first address some aspects of the data-processing (cf. also Fig. 3). It is followed by evaluating the deviations between the design-values of the waveguides and the actual realizations. We then comment on the observed differences over the full band (210–300 GHz), which we arbitrarily divided into 4 smaller subbands: 210–225 (i), 225–243 (ii), 243–261 (iii), and 261–300 (iv) GHz. Finally, we infer from these quantitative results the communication rate.

For the data shown in Fig. 6, the experimental and model results are both averaged, using a moving average postprocessing procedure with an averaging length much smaller than the length of the data. The experimental data consist of six frequency-sweep datasets for the long waveguide and two frequency-sweep datasets for each of the two short waveguides. The datasets for each waveguide were acquired subsequently and in the present analysis are averaged before the moving average postprocessing procedure; cf. Fig. 5. In this way, we smooth out fast fluctuations introduced by standing waves, caused by the large impedance mismatch between photo-mixers and diagonal-horn antennas. After this, we normalize the data to enable a mutual comparison. The reason for this is that the setup shown in Fig. 1(a) determines essentially a relative transmission in comparison to the situation when no field is transmitted through the waveguide. Unfortunately, a reference calibration procedure is generally difficult with this type of setup due to the sensitive optical alignment and the difficulty to measure absolute powers.
at these high frequencies. Nevertheless, the calculated S-parameters from the model permit an analysis of the absolute values of the signal loss of the transmitted field.

We find that in order to bring consistency between the measurements and the modeling results, we have to assume a smaller rectangular waveguide feedpoint of the diagonal-horn antenna than the waveguide connecting the two diagonal-horn antennas (as shown in Fig. 4). The most important experimental indication justifying this assumption is that for our three different waveguides, using the same diagonal horn antennas, we measure consistently the same onset of transmission of about $f_{\text{min}} = 200$ GHz. Since the waveguide fabrication is not reproducible with this precision, for instance, a deviation within the machining precision of ±5% of the waveguide, a-side would shift $f_{\text{min}}$ already by ±20 GHz; this suggests that the rectangular waveguide feedpoint of the diagonal-horn antenna is the bottleneck for the transmission. Based on our measurements, it has to have a size of the order of $a = c/(2f_{\text{min}}) \sim 750 \mu$m. This corresponds to a deviation of 50 μm from the nominal design of 800 μm for the a-side introduced earlier and is consistent with the uncertainty expected from the waveguide machining. We assume, therefore, that the onset of transmission in all three waveguides is due to the size of the entry- and exit-orifice of the horn antennas.

Furthermore, in order to explain unambiguously the measured transmission spectrum, we have to assume for the experimental waveguides slightly different dimensions than designed. For the long waveguide with length $l = 79.2$ mm, a modified cross section $a = 833.010 \mu$m. Similarly, for the shorter waveguides with length $l = 39.6$ mm, a modified cross section $a = 856.285 \mu$m. While choosing these new values for $a$ in the waveguide, we keep in the model the diagonal-horn antenna feedpoint waveguide fixed to the nominal value of 800 μm for simplicity. In making the latter simplification, we accept a small underestimate of the input impedance of the diagonal-horn antenna, which turns out to be negligible for our analysis. Note that the decimal numbers of the $a$-values indicate the exact input used for modeling. Although the decimal numbers specify just a small length variation relative to the wavelength, slightly changing them modifies also the modeling results. "This result is expected for a microwave device which is much longer than the wavelength and has a large impedance mismatch. It causes a sizeable standing wave ratio which is strongly influenced even by such small relative length variations, modifying the electric field amplitude at the detector. Additionally, we assume that the waveguides are shorter by in total about 11 μm. This amounts to 4% of the height of the diagonal-horn waveguide flange, which is mechanically squeezed during the

FIG. 5. Raw data (thin transparent line) to averaged data (thick line) processing for the case of the long-waveguide; cf. Fig. 6(a). In this case, the raw data comprise six traces, which were acquired subsequently and then averaged, whereas the thick line is the result of the moving average postprocessing procedure, as described in the text.
mounting based on our experience, due to the compression of the diagonal-horn antenna waveguide flange using the screws shown on the clamp in Fig. 1(d) in the dashed area. This length modification has been included in our model through shortening the waveguide length \( l \) in Eqs. (5). With these adjustments, the results shown in Fig. 6 can now be discussed including the comparison between experimental and modeled results.

As mentioned before, we divide the results for the transmission in four subbands 210–225 (i), 225–243 (ii), 243–261 (iii), and 261–300 (iv) GHz. This choice has no physical basis but was suggested by the pattern observed in both the modeling and the experiment, in particular for the long waveguide. For this waveguide with length \( l = 79.2 \) mm, Figs. 6(a) and 6(b), the transmission shows three maxima in the regions (i) and (ii) and is slightly flatter in regions (iii) and (iv) but still showing pronounced features. All observed features in the measurement in (a) can be qualitatively and mostly also quantitatively related to the pattern found by the model shown in panel (b). However, the peak which we observe in the measurement between regions (ii) and (iii) is not found from the model. We assume that, given the large impedance mismatch between the photo-mixers and the diagonal-horn antenna, together with the overall length of the diagonal horn and waveguide device, much larger than the transmitted wavelength, that transmission features appear, which are not exactly reproduced by our model. In this case, not only the setup but also the modeling is very sensitive to small length variations, which would introduce similar features. We suggest that this is the most likely explanation for this particular transmission feature.

For the shorter waveguides of length \( l = 39.6 \) mm, the overall transmission is much flatter and shows less pronounced maxima in the spectrum. Similar to the long waveguide, the regions (i) and (ii) in the model for the short waveguide, Fig. 6(d), show three peaks. These can only be partly assigned in the measured transmission of waveguide 2, shown in Fig. 6(c), and of waveguide 3, shown in the same panel. The transmission of the latter one (blue-dashed line) compared to waveguide 2 (black solid line) shows generally a smoother frequency response with less pronounced features. In these waveguides, the transmission in the region (ii) to (iii) is first slightly decreasing and then in region (iv) slightly increases again, separated from a small dip between regions (iii) and (iv). At least, this trend is reproduced by the model. This is clearly manifest for waveguide 2 for which also the dip is slightly deeper than that for waveguide 3. In the latter case, it is almost not distinguishable from the other ripples in the transmission. In region (i), the model predicts a dip also at around 220 GHz, which is not obtained in the measurement. Similar to the case for the long waveguide, we also suspect here the strong sensitivity to length variations of the waveguide, leading to standing wave patterns in the setup.

We would like to add that the short period oscillations in the short waveguides are reminiscent of universal conductance fluctuations (UCFs), studied earlier theoretically for light-scattering in waveguides.\(^{20}\) In the latter work, the central outcomes are correlation functions, which quantify the coherence of the fluctuating intensity pattern of the light traveling through the waveguide, leaving out both inelastic scattering and absorption which have the effect of weakening or even destroying the coherence. The latter effects cannot be neglected in our case due to our normal conducting waveguides. Nevertheless, we built the autocorrelation function out of the raw data of the amplitude fluctuations measured in our short and long waveguides and obtain a similar shape of the correlation function, as derived in the work of Feng et al.\(^{19}\) in our case, however, as a function of frequency lag, \( \Delta f \), instead of wavevector lag. We find that the amplitude autocorrelation functions for the short waveguides decay for \( \Delta f = 492 \) MHz to a value 1/e, whereas for the long waveguide, the same decay is already obtained for \( \Delta f = 334 \) MHz. The bare transmission between the two photo-mixers, i.e., without a waveguide in-between, also shows a fluctuating transmission, most likely due to internal reflections in the Si lens and standing-waves and needs to be disentangled. In this case, \( \Delta f = 550 \) MHz takes the largest value. Interestingly, we find that the cross correlation between the amplitude fluctuations of two independent measurements of the two different short waveguides yields a nonvanishing correlation, about half as large as the autocorrelation, obtaining \( \Delta f = 900 \) MHz and suggesting a strong coherence between them. Cross-correlating in the same way the amplitude fluctuations measured in the long waveguide with the ones in the short waveguides yields a much shorter coherence of \( \Delta f = 200 \) MHz and a much weaker correlation only about 17% of the autocorrelation. As mentioned in the work of Feng et al.,\(^{19}\) waveguides and microwaves are a versatile system to study UCFs, but concerning this aspect and the present status of our work, more work has to be performed in the future.

Finally, we address the communication rate of these waveguides. We calculate, using the measured transmission, the expected communication rate through the waveguides, based on Eq. (8) of Sec. V. The results for the different waveguides are shown as green traces in the panels along with the experimental results in Figs. 6(a) and 6(c). To achieve these plots, the central challenge is to calculate the power \( P \) in Eq. (8) at the input of the waveguide. From our model, we determine the electric-field coupling constant from the input to the output of the waveguide and the diagonal-horn antennae, i.e., \( S_{21} \), and multiply it with the measured and then normalized transmission. Since the model accounts for dissipative losses, we finally obtain the absolute transmission. From this, we calculate the power coupling and multiply it with the expected generated power at 235 GHz, about 1 \( \mu \)W,\(^{11,15}\) taking into account the operation parameters of the terahertz source. Note that alternative direct methods for power measurements of the two different short waveguides yields a nonvanishing correlation, about half as large as the autocorrelation, obtaining \( \Delta f = 900 \) MHz and suggesting a strong coherence between them. Cross-correlating in the same way the amplitude fluctuations measured in the long waveguide with the ones in the short waveguides yields a much shorter coherence of \( \Delta f = 200 \) MHz and a much weaker correlation only about 17% of the autocorrelation. As mentioned in the work of Feng et al.,\(^{19}\) waveguides and microwaves are a versatile system to study UCFs, but concerning this aspect and the present status of our work, more work has to be performed in the future.

We finish this section by comparing the possible communication rates we obtain, of the order of 1 bit per photon in the wideband coherent-state channel limit, with the limits derived by Caves and Drummond.\(^{1} \) We obtain this result using the theoretical framework described in Sec. V, which also explains the assumptions used in our derivation. From their theory, the maximum communication rate expected for a coherent-state channel is of the order of 2 bits per photon. They found that this maximum rate can only be achieved by experimentally realizing the “one quantum-one bit-one mode” strategy we have mentioned in the Introduction. This would be the case if \( P/\hbar f \sim C \sim f \). In our system, however, \( P/\hbar f \gtrsim C \gg f \). From this result, the implication for the practical realizable communication rate can be drawn from the analysis in the work of Caves and Drummond.\(^{1} \) Our results imply that for our particular waveguide geometry, the injected power, and used carrier frequencies, the rate at which quanta are transmitted down the channel is similar but still somewhat higher than the channel capacity and the carrier

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frequency is the slowest quantity. As a consequence, about one quantum per bit of information can be used, but far less than one bit per period (mode) is transmitted. This can be compensated by increasing the carrier frequency (at the same time reducing the waveguide dimensions to keep the single-mode character) and increasing the injected power $P$ with the goal to realize the ideal “one quantum-one bit-one mode” communication strategy.

V. CHANNEL CAPACITIES

A rectangular waveguide, as shown in Fig. 1(a), is often viewed as a component in a receiver system, which guides a signal to a detector. Alternatively, it can be analyzed in information theory as a channel to guide information, which can be decoded with a minimal amount of error. In classical physics, noise is introduced by signal loss in the channel or by coupling loss, such as when the signal is injected into the channel from an emitter. If quantum mechanics plays a role, for example, in the case of a coherent receiver, noise due to vacuum fluctuations has to be taken into account. For a signal carrier frequency $f$ with bandwidth $\delta f$, a noise power of $\sim hf\delta f$ will contribute. This contribution will be significant for signals with high-frequency carriers and a wide bandwidth of the order of $\delta f \sim f$. Both contributions, classical and quantum, have the effect of reducing the signal-to-noise ratio (SNR) at the receiver.

The physics of information theory has been formulated by Shannon, creating the basis of quantum information theory. \(^1\) The main interest is in the maximum rate at which information can be sent through a channel, while being still decodable without errors. A quantitative measure is the maximum channel capacity $C_{ch}$ expressed in bits/s. It is derived from the information entropy in the Shannon-theory through the source and channel coding theorems. \(^2\) For the case of a lossless channel and a negligible thermal photon population, the classical channel capacity reads

$$C_{ch,cl} = \delta f \log_2 \left( 1 + \frac{P}{N\delta f} \right),$$

(6)

with $P$ being the transmitted power through the channel and $N$ being the noise power per hertz. In classical physics, there is no lower limit on $N$, i.e., the noise can be infinitesimally small. Consequently, the channel capacity would tend to infinity. This unphysical result has motivated a number of theoretical studies to determine the proper physical limit of the channel capacity, reviewed by Caves and Drummond \(^3\) and by Yuen and Ozawa. \(^4\) For a quantum channel, cf. the later Eq. (9), Yuen and Ozawa \(^4\) derived in addition the limits of the average transmitted power $P$. Their work derives the maximum of the von Neumann information entropy, quantifying the maximum number of available input states to the channel, evidencing that it is classically an unbounded value but not quantum-mechanically. A heuristic method to impose a limit to $C_{ch,cl}$ is to state $N \sim hf$ so that

$$C_{ch,C} = \delta f \log_2 \left( 1 + \frac{P}{hf\delta f} \right).$$

(7)

The subscript $C$ refers to a coherent state. The second part of the term between the brackets of Eq. (7) is then the mean photon occupation number, $n = P/(hf\delta f)$, and the power $P$ can be understood as a classical quantity. In this limit, Eq. (7) already gives the correct channel capacity for a free-space single coherent state channel with a narrow bandwidth, $\delta f \ll f$. This expression yields a maximum capacity of $\approx 0.586$ bits per photon. It can be determined by expressing Eq. (7) as a normalized capacity, $C_{ch,C} \rightarrow C_{ch,C}/(\delta f h)$, followed by finding its maximum. \(^5\)

In practice, a wideband capacity is often relevant, for example, when many longitudinal modes are present within one transverse mode by frequency multiplexing. In this case, $\delta f \sim f$ and Eq. (7) is for a coherent state no longer valid since $n \ll 1$. Including the frequency dependence of the photon energy, Caves and Drummond \(^3\) derived the wideband limit of the single frequency-multiplexed coherent state channel, yielding the capacity

$$C_{WB, ch}^{WB} = \frac{1}{\ln(2)} \sqrt{\frac{2P}{h}}$$

(8)

and, hence, $A \times 2.0403$ bits per photon.

For a single number-state wideband channel, the channel capacity becomes

$$C_{ch,N}^{WB} = \frac{\pi}{\ln(2)} \sqrt{\frac{2P}{3h}}$$

(9)

and yields, therefore, $A \times 3.7007$ bits per photon. Equation (9) is determined by the application of the so-called Holevo bound. \(^1, 30, 45–48\) which quantifies the maximal amount of information that can be obtained at the output of the channel using the concept of mutual information transfer. We would like to add that the same equation [Eq. (9)] has been derived in the work of Yuen and Ozawa by relaxing the finiteness assumptions in the Holevo bound and considering instead an infinite-dimensional input/output alphabet for the communication. A detailed discussion about the history of these approaches is given in the work of Caves and Drummond. \(^4\)

The prefactor $A$ has to be determined separately for different types of waveguides and field-patterns. In Eqs. (8) and (9), $A = 1$ for a free-space channel. For a full-height rectangular waveguide with dimensions $a = 2b$, cf. Figs. 1(a) and 2(d), one gets $A = \cos(\theta_k)$. Moreover, $\omega \cos(\theta_k)$ quantifies the reduction in longitudinal group velocity in the waveguide due to reflection at the waveguide walls [refer to the work of Giovannetti et al. \(^5\) and Fig. 1(a)]. The angle of reflection is given by $\theta_k = \arccos(k_z/|k|)$ for the fundamental TE$_{10}$ mode, where $k = (\pi/2a, 0, 2\pi\lambda_D/a)$, with $\lambda_D$ being the wavelength in the waveguide. Note that the wavelength in the waveguide $\lambda_D > \lambda$ is always larger than the wavelength in free space since $\lambda_D = 2\beta/\beta$, with $\beta = (\sqrt{(a/c_0)^2} - (\pi/a)^2)$ being the complex propagation constant. Consequently, $\theta_k \rightarrow \pi/2$ for long wavelengths approaching the waveguide cutoff $\lambda \sim 2a$, i.e., $\omega/\omega_0 \sim \pi/a$, where $\omega_0$ diverges and $\beta \rightarrow 0$, resulting in a vanishing group velocity, $(d\beta/da)^{-1} = c_0\beta/a\pi$. In other words, the channel capacity vanishes in this case since no information can be transmitted anymore.

This overview of formulas for the channel capacities demonstrates that the value depends theoretically on the type of the waveguide. A convenient way to study the predictions of Eqs. (8) and (9) experimentally is to realize a frequency-multiplexed channel, which splits the available bandwidth into small nonoverlapping frequency bins, which together carry a total transmitted power $P$. Furthermore, dependent on the type of the channel, one has to realize the optimal photon-occupation number for each bin in order to achieve the maximum capacities (8) and (9). Optimal photon-occupation number distributions for the number-state and coherent-state channels are summarized in the work of Caves and Drummond. \(^4\) For a single-mode waveguide, as studied by us, each frequency bin then...
represents an independent longitudinal channel with different $\theta_k$ within the same transversal mode, in this case the fundamental $\text{TE}_{10}$ mode.

In the practical case of a lossy waveguide, as in our experiment, illustrated by the black and red transmission curves shown in Fig. 1(b), not all photons of the electromagnetic field supplied at the input of the waveguide will reach the output. For the capacity of a number-state channel, this creates a difficult theoretical problem related to the exact form of the input information entropy. This problem is explained in detail by Giovannetti et al.\textsuperscript{9} and recently in the work of Ernst and Kliese\textsuperscript{23} by considering a general quantum channel. This recent work studies as a proof-of-principle the regularization of the maximum pure-state input-output fidelity of a quantum channel. We expect that, for the capacity of a quasiclassical coherent state channel, Eq. (8), reasonable conclusions are still possible even in the presence of loss. Therefore, we focus on this type of channel while conducting our experiment.

VI. FREE SPACE QUANTUM OPTICS EMPLOYING JOSEPHSON PHOTONICS AND WAVEGUIDES

This section addresses the conceptual framework of realizing free space quantum optics using recent achievements in Josephson photonics.\textsuperscript{30,31} In particular, the experimental works reported by Rolland et al.\textsuperscript{32} and Grimm et al.\textsuperscript{33} implement an only battery-powered Josephson junction which is strongly coupled to a single mode, realizing a single photon source. The experiment in the work of Westig et al.\textsuperscript{34} reports two-mode amplitude squeezing below the classical limit using also an only battery-powered Josephson junction, but this time weaker coupled to two modes of different frequencies. It is important mentioning that Grimm et al.\textsuperscript{33} realized a NbN based Josephson junction that could in principle generate radiation in the frequency window employed in our work, extending the frequency range compared to only aluminum-based circuits.

For a given frequency and an adequate choice of the waveguide and diagonal-horn antenna dimensions, we like to recall that the waveguide cut-off wavelength scales as $\lambda_{min} \sim 2a$, with $a$ being the long side of the rectangular waveguide and $b = a/2$ being the short side of the waveguide. It is then a straightforward microwave engineering task to excite a rectangular waveguide with a Josephson device by using a planar antenna.\textsuperscript{35} The latter antenna design is compatible with coplanar waveguides frequently used in circuit quantum-electrodynamics. A second way to excite the fundamental waveguide mode in an even simpler way, but only working for lower gigahertz frequencies to about 60 GHz, uses a coaxial cable fixed in a back-short waveguide piece along the $E$-plane. For such a transition to work with low return loss, the coaxial cable inner core is fixed at a distance $-b$ away from the back-short and extending a distance $-b/2$ into the waveguide. The latter coaxial cable to waveguide transition is a standard and commercially available microwave element.

Connecting the aforementioned Josephson photonic devices in this way to the waveguide field, one takes advantage of the flexible way of generating tailored photonic fields in Josephson devices through strong charge-light coupling. At the same time, one could radiate these fields into free space by using the diagonal-horn antenna where quantum optic techniques provide to manipulate and measure the fields in a more flexible way than in a circuit configuration. For instance, for a free-space field, one can then exploit additionally the polarization degree of freedom as reviewed in more detail by Sanz et al.\textsuperscript{34} Free-space ultralow-loss coupling to additional quantum devices, for instance to build a network, shows another benefit of this scheme.\textsuperscript{43,44} In order to minimize the signal loss in the immediate vicinity of the Josephson device, important to realize a number-state channel or to preserve a high degree of amplitude squeezing contained in a two-mode field, the rectangular waveguide should be made of a superconducting material or has to be coated with a superconductor up to a thickness much larger than the electromagnetic penetration depth.

VII. CONCLUSION

To conclude, we have measured the transmission of different length rectangular full-height waveguides between 160 GHz and 300 GHz, connected to diagonal-horn antennas and optically coupled to a coherent detection scheme using a high-impedance source and detector with a high dynamic range. A detailed but still simple enough electromagnetic model includes the optical properties of the diagonal-horn antennas, the dispersion relations of the waveguides, and the optical properties of the source and detector together with the coupling to those. The model accounts for most of the measured features. The central outcomes of our measurements are highly resolved transmission functions, which reflect the frequency dependent impedance of the diagonal-horn and waveguide assembly, and the coupling mismatch to the source and the detector. A careful estimation of the channel capacity obtains a rate of 1 bit per photon in the wideband channel limit of a coherent state.

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