Compton-thick AGNs in the NuSTAR Era. II. A Deep NuSTAR and XMM-Newton View of the Candidate Compton-thick AGN in NGC 1358

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Abstract

We present the combined NuSTAR and XMM-Newton 0.6–79 keV spectral analysis of a Seyfert 2 galaxy, NGC 1358, which we selected as a candidate Compton-thick (CT) active galactic nucleus (AGN) on the basis of previous Swift/BAT and Chandra studies. According to our analysis, NGC 1358 is confirmed to be a CT-AGN using physically motivated models, at >3σ confidence level. Our best fit shows that the column density along the line of sight of the obscuring material surrounding the accreting supermassive black hole is \(N_H = (1.96\pm2.80) \times 10^{24} \text{ cm}^{-2}\). The high-quality data from NuSTAR give the best constraints on the spectral shape above \(\sim10\) keV to date on NGC 1358. Moreover, by combining NuSTAR and XMM-Newton data, we find that the obscuring torus has a low covering factor \((f_c < 0.17)\), and the obscuring material is distributed in clumps, rather than uniformly. We also derive an estimate of NGC 1358’s Eddington ratio, finding it to be \(\lambda_{\text{Edd}} \sim 4.7_{-0.3}^{+0.3} \times 10^{-2}\), which is in acceptable agreement with previous measurements. Finally, we find no evidence of short-term variability, over a \(\sim100\) ks time span, in terms of both line-of-sight column density and flux.

Key words: galaxies: active – galaxies: individual (NGC 1358) – galaxies: nuclei – X-rays: galaxies

1. Introduction

The cosmic X-ray background (CXB; i.e., the diffuse X-ray emission observed between 0.5 and 300 keV) is thought to be mainly produced by obscured and unobscured active galactic nuclei (AGNs; e.g., Alexander et al. 2003; Gandhi & Fabian 2003; Gilli et al. 2007; Treister et al. 2009). Compton-thick (CT) AGNs (with absorbing column density \(N_H \geq 10^{24} \text{ cm}^{-2}\), where \(\sigma_T\) is the Thomson cross section) are supposed to contribute up to \(\sim10\%\) of the CXB intensity at its spectral peak \((\sim30\) keV; Ajello et al. 2008\) and are expected to be numerous (up to 50\% of the overall population of Seyfert 2 galaxies; see, e.g., Risaliti et al. 1999). However, as of today CT-AGNs have never been detected in large numbers, their observed fraction in the local universe being \(\sim5\%–10\%\) (see, e.g., Burlon et al. 2011; Ricci et al. 2015), significantly below the predictions of different CXB models \((\sim20\%–30\%\); see Ueda et al. 2014, and references therein). Nevertheless, it has been suggested that the small observed fraction of heavily obscured AGNs observed can be caused by the bias in detecting CT-AGNs in X-rays, even sampling the energy range above 10 keV (see, e.g., Burlon et al. 2011). Efforts to correct for this observational bias have recovered a fraction of \(\sim20\%\) of CT-AGNs, under some assumptions (see, e.g., Brightman & Nandra 2011; Burlon et al. 2011; Ricci et al. 2015). In Compton-thick AGNs, the spectrum is significantly suppressed at energies \(\leq10\) keV (Gilli et al. 2007; Koss et al. 2016), and the overall emission is dominated by the Compton hump at \(\sim30–50\) keV. Consequently, CT-AGNs at redshifts \(z > 1\) can be studied using one of the several facilities sampling the \(\sim0.5–10\) keV energy range, such as XMM-Newton, Chandra, Swift-XRT, and Suzaku (see, e.g., Georgantopoulos et al. 2013; Buchner et al. 2015; Lanzuisi et al. 2015), since the Compton hump of high-z sources is redshifted in the energy range covered by these instruments. For sources in the local universe \((z < 0.1)\), however, the proper characterization of heavily obscured AGNs requires an X-ray telescope sensitive above 10 keV. Thanks to the launch of the Nuclear Spectroscopic Telescope Array (NuSTAR; Harrison et al. 2013), which provides a two order of magnitude better sensitivity than previous telescopes at these energies (e.g., INTEGRAL and Swift/BAT; Winkler et al. 2003; Barthelmy et al. 2005), we can characterize the physical properties of heavily obscured AGNs with unprecedented accuracy (see, e.g., Baloković et al. 2014; Puccetti et al. 2014; Annuar et al. 2015; Marchesi et al. 2017b; Ursini et al. 2018). However, since a typical highly obscured AGN spectrum barely depends on the column density at \(\geq10\) keV but varies considerably at \(<10\) keV (see, e.g., Gilli et al. 2007), it is difficult to constrain the column density with NuSTAR alone. Consequently, XMM-Newton, as the best instrument in terms of effective area in \(0.3–10\) keV \((\sim10\) times larger than Swift-XRT and \(\sim2\) times larger than Chandra\), is the ideal instrument to complement NuSTAR strength in characterizing heavily obscured AGNs.

Indeed, the study of single targets using NuSTAR or combining NuSTAR and other lower-energy X-ray observatories (e.g., XMM-Newton and Chandra) has already been shown to be strategic for characterizing heavily obscured AGNs and understanding their physical properties. For example, NGC 1448 was observed and identified as a CT-AGN in X-rays for the first time using NuSTAR and Chandra (Annuar et al. 2017). The source was too faint (intrinsic 2–10 keV luminosity \(L_{\text{int},2–10\text{ keV}} = (3.5–7.6) \times 10^{40} \text{ erg s}^{-1}\) to be identified by Swift/BAT, even using its deepest 104-month maps, and was only detected in one out of five Swift-XRT observations. Another example is the analysis of NGC 1068 reported in Bauer et al. (2015). In this work, the authors used NuSTAR to characterize with unprecedented quality this
lately studied CT-AGN, putting much stronger constraints on the high-energy spectral shape of NGC 1068. The obscuration observed in AGNs across the electromagnetic spectrum, from the X-ray to the optical and infrared, is usually explained with a parsec-scale, torus-like structure of the high-energy spectral shape of NGC 1068. Consequently, in the past two decades several torus models, based on Monte Carlo simulations, have been developed to characterize CT-AGN X-ray spectra (Matt & Fabian 1994; Ikeda et al. 2009; Murphy & Yaqoob 2009; Brightman & Nandra 2011; Liu & Li 2014; Furui et al. 2016; Baloković et al. 2018). All these models assume a continuous distribution of the obscuring material, but with different assumptions on the geometry of the torus. In particular, in the models proposed by Ikeda et al. (2009), Brightman & Nandra (2011), and Baloković et al. (2018), the half-opening angle of the torus, i.e., the torus covering factor, is a free parameter, thus allowing us to put constraints on the typical torus geometry. Given the intrinsic complexity of these models and the multiple free parameters involved, using them in full capacity requires high-quality X-ray spectra, with excellent statistics on a wide energy range, i.e., between 2 and 100 keV: as of today, such requirements can be satisfied only by a joint NuSTAR and XMM-Newton observation.

In this work we present the results of a deep, 50 ks joint NuSTAR and XMM-Newton observation of NGC 1358, a nearby Seyfert 2 galaxy and a CT-AGN candidate. The paper is organized as follows: In Section 2 we present the selection technique that brought us to classify NGC 1358 as a new candidate CT-AGN, and we report the NuSTAR and XMM-Newton data reduction and spectral extraction process. In Section 3, we describe the different models, both phenomenological and physical, that have been used to fit the spectra, as well as the results of the spectral analysis. In Section 4 we compare our results with previous ones, derive the source Eddington ratio, and discuss the constraints on the geometry and clumpiness of the obscuring materials. All reported errors are at 90% confidence level, if not otherwise stated. Standard cosmological constants are adopted as follows: \(H_0 = 70 \text{ km s}^{-1} \text{Mpc}^{-1}\), \(\Omega_b = 0.0\), and \(\Lambda = 0.73\).

## 2. Observation and Data Analysis

NGC 1358 (\(z \approx 0.013436\); Theureau et al. 1998), is a Seyfert 2 galaxy detected in the 100-month BAT catalog (with a 7.8\(\sigma\) significance; Segreto et al. 2018, in preparation), a catalog of \(\sim 1000\) AGNs detected by Swift-BAT in the 15–150 keV band.

In Marchesi et al. (2017a), we describe a technique developed to select highly obscured AGN candidates from the BAT sample, using the following criteria:

1. Lack of a 0.5–2.4 keV, ROSAT/RASS (Boller et al. 2016) counterpart. For objects located outside the Galactic plane (i.e., having Galactic latitude \(|b| > 10^\circ\), the lack of ROSAT counterparts already implies a minimum AGN column density \(\log(N_H) \sim 23\) (see, e.g., Figure 2 in Koss et al. 2016).
2. Seyfert 2 galaxy optical classification, i.e., the source must have an optical spectrum without broad (FWHM \(\geq 2000 \text{ km s}^{-1}\)) emission lines. It has been shown (see, e.g., Marchesi et al. 2016, and references therein) that Seyfert 2 galaxies are more likely to be obscured than Seyfert 1 ones. Furthermore, there are no known Seyfert 1 galaxies that are Compton thick\(^5\) (see, e.g., Ricci et al. 2015).
3. Low redshift (\(z < 0.04\)). Due to selection effects, the vast majority of BAT-selected CT-AGNs are detected in the nearby universe: for example, 47 out of 55 CT-AGNs reported in Ricci et al. (2015) are located at \(z < 0.04\).

Following these criteria, we obtained a snapshot (10 ks) Chandra observation for a sample of seven sources, and we performed a first measurement of their fundamental spectral parameters, particularly the power-law photon index, \(\Gamma\), and the column density, \(N_H\). NGC 1358 was found to be the most obscured object in our sample, having line-of-sight column density \(N_H = 1.05^{+0.42}_{-0.36} \times 10^{24} \text{ cm}^{-2}\), thus making it a candidate CT-AGN, although only at a 1\(\sigma\) confidence level, due to the low-quality of the Chandra spectrum.

To further investigate this new candidate CT-AGN, we proposed a joint deep NuSTAR (50 ks) and XMM-Newton (48 ks) follow-up observation, which was accepted in NuSTAR Cycle 3 (proposal ID 3258, PI: Marchesi). We report a summary of the two observations in Table 1.

### 2.1. NuSTAR Observation

NGC 1358 was observed by NuSTAR on 2017 August 1 (ObsID 60301026002); the net exposure time is 50 ks. The observation actually took place in a 96.9 ks time span and was divided into 16 (~3 ks) intervals. The nonexposed time between each interval is when the target is occulted by the Earth.

The NuSTAR data are derived from both focal plane modules, FPMA and FPMB. The raw files are calibrated, cleaned, and screened using the NuSTAR nupipeline script version 0.4.5. The NuSTAR calibration database (CALDB) used in this work is the version 20161021. The ARF, RMF, and light-curve files are obtained using the nuproducts script.

For both modules, the source spectrum is extracted from a 25° circular region, corresponding to \(\approx 40\%\) of the encircled area.

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\(^5\) There are sources that are Compton-thick but with ambiguous activity classification, e.g., NGC 424 (aka Tololo0109-383).

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### Table 1

Summary of NuSTAR and XMM-Newton Observation

| Instrument | ObsID  | Start Time (UTC) | End Time (UTC) | Exposure Time (ks) | Count Rate \(^a\) (10\(^{-2}\) counts s\(^{-1}\)) |
|------------|-------|-----------------|---------------|-------------------|-----------------------------|
| NuSTAR     | 60301026002 | 2017-08-01T03:41:09 | 2017-08-02T06:36:09 | 50 | 2.32 ± 0.07 2.28 ± 0.07 |
| XMM-Newton | 0795680101 | 2017-08-01T17:05:27 | 2017-08-02T06:03:10 | 48 | 0.98 ± 0.05 0.91 ± 0.05 3.68 ± 0.15 |

Note.

\(^a\) The reported NuSTAR net count rates are those of the FPMA and FPMB modules between 3 and 79 keV, respectively. The reported XMM-Newton net count rates are those of the MOS1, MOS2, and pn modules in 0.6–10 keV, respectively.
energy fraction at 10 keV, centered on the source optical position. We then extract a background spectrum for each module, choosing a 30' circular region located near the outer edges of the field of view, to avoid contamination from NGC 1358. We group the NuSTAR spectra with a minimum of 15 counts per bin with the grppha task. The signal of both modules is >3σ in the 3–79 keV band.

2.2. XMM-Newton Observation

The XMM-Newton observation was taken quasi-simultaneously to the NuSTAR one starting ~12 hr after the NuSTAR one, but ending at the same time (due to the gaps between observing intervals in NuSTAR). XMM-Newton data have been reduced using the Science Analysis System (Jansen et al. 2001) version 16.1.0. A total of 13 ks of XMM-Newton modules MOS1 and MOS2 and 30 ks of pn observations were affected by a strong background flare; therefore, we decided to exclude that part of the observation from our analysis. Consequently, the total net XMM-Newton exposure time of our observation is 101 ks. The source spectra are extracted from a 15' (corresponding to ≃70% of the encircled energy fraction at 1.5 keV) circular region, while the background spectra are from an 80' circle located nearby the source. We visually inspected the XMM-Newton image to avoid contamination to the background from sources nearby NGC 1358. All three modules, MOS1, MOS2, and pn, are jointly used in the spectral modeling, and their normalizations are tied together assuming that their cross-calibration uncertainties are marginal.

3. Spectral Modeling Results

We use XSPEC (Arnaud 1996) v12.9.1 to fit the spectrum and rely on the χ² statistic for the optimization of the spectral fit. The photoelectric cross sections for all absorption components used here are derived from Verner et al. (1996), adopting an element abundance from Anders & Grevesse (1989). The Galactic absorption column density is N_Gal = 3.83 × 10²⁰ cm⁻² (Kalberla et al. 2005). The metal abundance is fixed to solar.

Following a standard approach in analyzing heavily obscured AGNs, we first fit our data using different phenomenological models, particularly the pexrav one (Magdziarz & Zdziarski 1995). We then move to more accurate self-consistent models, based on Monte Carlo simulations, which are specifically developed to treat the spectra of heavily obscured AGNs: the physical models we use in this work are MYTorus (Murphy & Yaqoob 2009) and borus02 (Baloković et al. 2018). We report the results of our analysis in the following sections.

3.1. Phenomenological Models

3.1.1. Absorbed Power Law

We initially fit our data with a simple phenomenological model, comprising a power law (zpowerlw in XSPEC) absorbed by intervening gas modeled with zphabs. We also add a Gaussian (zgauss) to model the Fe Kα fluorescent emission line (E_Kα = 6.4 keV); we assume the line to be narrow, fixing the line width σ to 50 eV, since there is no statistical improvement in fits if the parameter is left free to vary. We also add a second, unabsorbed power law, to model the fractional AGN emission, which is not intercepted by the torus on the line of sight, and/or the scattering emission that is deflected, rather than absorbed by the obscuring material. Here, and elsewhere in the paper, the photon index of the scattered component is tied to the one of the main power law. The scattered component is usually less than 5%–10% of the main one (see, e.g., Marchesi et al. 2018). We denote this fraction as f_s and we model it with a constant (constant2). Furthermore, we add to the fit a thermal component, namely, mekal (Mewe et al. 1985), to model the soft excess observed below 1 keV, and potentially due to either star formation processes and/or thermal emission from a hot interstellar medium. The temperature and the relative metal abundance in mekal are both left free to vary.

The first model (hereafter “Model A”), in XSPEC nomenclature, is therefore

\[ \text{Model A} = \text{constant}_1 \times \text{phabs} \times (\text{zphabs} \times \text{zpowerlw}) \]

+ zgauss + constant2 × zpowerlw + mekal, \]

where constant1 represents the cross-calibration between different instruments, noted as C_NuS/XMM. In our fits, the cross-calibration between different modules of the same instrument is fixed to 1. phabs is applied here to model the Galactic absorption.

We report in Table 2 the best-fit results for the simple phenomenological model applied to the joint NuSTAR–XMM-Newton spectrum. The best-fit photon index is Γ = 1.14 ± 0.13, the column density is N_H = 0.95 ± 0.11 × 10²⁴ cm⁻². While the best-fit reduced χ² of model A is statistically acceptable, being χ² = χ²/degree of freedom (dof hereafter) = 256/240 = 1.07, standard absorption components in XSPEC, such as zphabs, fail to characterize the spectral complexity of heavily obscured AGNs like NGC 1358 properly. Therefore, a more physical model needs to be applied.

3.1.2. Including a Reflection Component

Obscured AGN X-ray spectra have historically been modeled using the pexrav model (Magdziarz & Zdziarski 1995). pexrav is used to model an exponentially cutoff power-law spectrum reflected from the neutral slab. We first test the model with a pure reflector by setting the reflection scaling factor in pexrav to be R = −1; this models a heavily obscured (N_H > 10²⁵ cm⁻²) source whose spectrum is dominated by the reflection from the back side of the torus. The fit shows that the photon index is Γ = 1.30 ±0.05 and χ²/dof = 349/242. Such a large reduced χ² suggests that a pure reflector is not enough to describe the spectrum. Therefore, we follow the method described in, e.g., Ricci et al. (2011) by using the complete pexrav model, which includes an intrinsic cutoff power law by setting the reflection scaling factor R to be greater than 0.

The model in XSPEC is described as follows:

\[ \text{Model B} = \text{constant}_1 \times \text{phabs} \times (\text{zphabs} \times \text{pexrav}) \]

+ zgauss + constant2 × zpowerlw + mekal, \]

\[ (2) \]

The components are those described previously in Section 3.1.1, except for the main power law, which is replaced by pexrav. The inclination angle i, i.e., the angle between the axis of the AGN (normal to the disk) and the observer line of sight, which is a free parameter in pexrav, is fixed at i = 60° (i.e., \( \cos i = 0.5 \)); we find no significant change in the best-fit statistic and in the other parameters when
Table 2
Summary of Best Fits of XMM-Newton and NuSTAR Data Using Different Models

| Model          | phenom | pexrav | MYTorus (Coupled) | MYTorus (Decoupled Face-on) | MYTorus (Decoupled Edge-on) |bonus02 |
|----------------|--------|--------|-------------------|-----------------------------|-----------------------------|--------|
| $\chi^2$/dof  | 256/240 | 231/240 | 231/239           | 230/239                     | 220/239                     |222/238 |
| $C_{\text{lin}}$ | 1.06±0.12 | 1.13±0.13 | 1.12±0.15         | 1.13±0.15                   | 1.17±0.16                   |1.16±0.12 |
| $\Gamma$    | 1.14±0.13 | 1.59±0.11 | 1.52±0.17         | 1.56±0.14                   | 1.85±0.23                   |1.79±0.04 |
| $N_H$ b      | 0.92±0.11 | 0.76±0.09 | 0.92±0.11         | 0.92±0.11                   | 0.92±0.11                   |...     |
| norm$^{-1}$  | 0.03±0.02 | 0.04±0.01 | 0.13±0.06         | 0.20±0.13                   | 1.61±1.18                   |1.26±0.04 |
| $\text{NH}_{\text{eq}}$ | ... | ... | 30.2±3.53 | ... | ... |... |
| $\theta_T$ c  | ... | ... | ... | ... | ... |... |
| $A_{\text{ob}}$ | ... | ... | 62.53±3.53 | ... | ... |... |
| $A_3$        | ... | ... | 1.03±0.55 | 0.78±0.17 | 0.23±0.18 |... |
| $A_{\text{H}}$  | ... | ... | ... | ... | 2.40±0.14 |2.40±0.12 |
| $f_c$ 10$^{-2}$ | 1.69±0.70 | 1.92±0.70 | 0.08±0.14 | 0.12±0.36 | 0.05±0.02 |0.05±0.01 |
| $kT^d$     | 0.49±0.09 | 0.49±0.10 | 0.58±0.07 | 0.57±0.12 | 0.58±0.09 |0.52±0.06 |
| abund$^e$   | 0.08±0.08 | 0.07±0.09 | 0.03±0.04 | 0.04±0.05 | 0.11±0.18 |0.05±0.08 |
| $F_{\text{2-10}}$ | 4.16±0.23 | 4.09±0.26 | 4.03±0.19 | 4.03±0.19 | 3.84±0.32 |3.87±1.11 |
| $F_{10-40}$ | 8.22±0.27 | 8.68±0.23 | 8.48±0.29 | 8.55±0.13 | 8.51±0.29 |8.51±0.46 |
| $L_{2-10}$ | 0.116±0.005 | 0.07±0.01 | 0.28±0.02 | 0.34±0.03 | 2.06±0.11 |1.77±0.10 |
| $L_{10-40}$ | 0.30±0.01 | 0.11±0.12 | 0.48±0.03 | 0.49±0.03 | 2.23±0.12 |2.09±0.12 |

Notes. We summarize here the best fits of joint NuSTAR–XMM-Newton spectra using different models referred to in Section 3. We also report the statistics and degrees of freedom for each fit.

a $C_{\text{lin}} = C_{\text{NuST}/XMM}$ is the cross-calibration between NuSTAR and XMM-Newton.

b Line-of-sight column density in phenomenological models in 10$^{24}$ cm$^{-2}$.

c Normalization of components in different models at 1 keV in photons keV$^{-1}$ cm$^{-2}$ s$^{-1}$.

d Angle between the axis of the torus and the edge of the torus in degrees, where the covering factor $f_c = \cos(\theta_{\text{tor}})$.

e Temperature in the thermal component mK in keV.

f Abundance in the thermal component mKAl.

g Flux between 2 and 10 keV in 10$^{-14}$ erg cm$^{-2}$ s$^{-1}$.

h Flux between 10 and 40 keV in 10$^{-12}$ erg cm$^{-2}$ s$^{-1}$.

i Intrinsic luminosity between 2 and 10 keV in 10$^{34}$ erg s$^{-1}$.

j Intrinsic luminosity between 10 and 40 keV in 10$^{35}$ erg s$^{-1}$.

allowing $i$ to vary. The cutoff energy of pexrav is fixed at 500 keV, to be consistent with the MYTorus model, which we will extensively discuss in the following section.

When leaving the reflection scaling factor $R$ in pexrav free to vary, we obtain a best-fit value of $R > 4$ (such a large reflection scaling factor is also found by Ricci et al. 2011, in heavily obscured AGNs), although we are not able to put any constraint on the parameter 90% confidence uncertainties. Such a result would point toward a reflection-dominated scenario, where most of the observed emission comes from the reflected component, while the direct emission from the accreting SMBH is absorbed by the heavily obscuring material along the line of sight. A larger scaling factor can also be interpreted as the geometry of reflected material being more like a torus than a disk. Since $R$ is not constrained when left free to vary, we decided to complete our spectral analysis fixing the reflection scaling parameter to $R = 4$. Here we are modeling a process in which the intrinsic emission and the reflection from the back side are obscured by the same circumnuclear material.

We report in Table 2 the best-fit parameters for the analysis of the joint NuSTAR–XMM-Newton spectra using model B. The photon index is $\Gamma = 1.59_{-0.11}^{+0.11}$. The best-fit column density is $N_H = 0.76_{-0.09}^{+0.04} \times 10^{24}$ cm$^{-2}$. In agreement with what we found using Model A, the source is near the threshold of CT-AGNs. We present the unfolded $\text{NuSTAR}$ and $\text{XMM-Newton}$ spectrum of NGC 1358, fitted with model B and the ratio between data and model, in Figure 1.

In summary, both phenomenological models suggest that obscuration is near the Compton-thick threshold, such that the source cannot be confirmed as a CT-AGN at $>3\sigma$ confidence level. However, the photon indices obtained above are far from the typical value observed in AGNs ($\Gamma \sim 1.8$; see, e.g., Marchesi et al. 2016), showing that some components may not be well described by the above phenomenological models. Therefore, more physically motivated models are needed to describe the spectra and extract the physical and geometrical properties of NGC 1358.

3.2. Physical Models

3.2.1. MYTorus

The first physically motivated model applied in our analysis is MYTorus (Murphy & Yaqoob 2009; Yaqoob 2012; Yaqoob et al. 2015). The basic geometry of the MYTorus model consists of a torus that has a fixed half-opening angle, $\theta = 60^\circ$, with a circular cross section.

An advantage of the physically motivated MYTorus model is that the main components observed in the spectrum of an obscured AGN can be treated self-consistently. More in detail, the MYTorus model is composed of three parts: the direct
continuum, the Compton-scattered component, and fluorescent lines. The direct continuum, which is also called zeroth-order continuum, is the line-of-sight observed continuum, i.e., the intrinsic X-ray continuum as observed after the absorption caused by the torus. In MYTorus, this first component is a multiplicative factor (a multiplicative table in XSPEC), which is applied to the intrinsic continuum. The second component is the scattered continuum, and models those photons that are Compton-scattered into the observer line of sight by the gas in the environment of the SMBH. If the covering factor of the torus differs significantly from the fixed MYTorus value, \( f_c = \cos(\theta) = 0.5 \), or if there is a non-negligible time delay between the intrinsic continuum emission and the Compton-scattered continuum one, i.e., the center region is not compact and the intrinsic emission varies rapidly, the two components could have different normalizations. To take these effects into account, the scattered continuum is multiplied by a relative normalization, which is noted as \( A_{\text{S}} \) (Yaqoob 2012). Finally, the third component models the most prominent fluorescent lines, i.e., the Fe K\( \alpha \) and Fe K\( \beta \) lines, at 6.4 and 7.06 keV, respectively. Analogously to \( A_{\text{S}} \), the relative normalization between the fluorescent lines and direct continuum is noted as \( A_L \). In XSPEC, \( A_{\text{S}} \) and \( A_L \) are implemented as two constant components before the additive tables, while the normalizations of the three components are set to be the same. Following previous works, the two relative normalizations are set to be equal, i.e., \( A_{\text{S}} = A_L \).

In XSPEC our model is described as follows:

\[
\text{ModelC} = \text{const} \_\text{C} \ast \text{phabs}\ast
\text{mytorus}\_E\_\text{zero}\_\text{v00}.\text{fits} \ast \text{zpowerlw}
+ A_{\text{S}} \ast \text{mytorus}\_\text{scattered}\_H\_500\_\text{v00}.\text{fits}
+ A_L \ast \text{mytl}\_V000010n\_Ep0000H500\_v00.\text{fits}
+ \text{const} \_2 \ast \text{zpowerlw} + \text{mekal}),
\]

where \text{mytorus}\_E\_\text{zero}\_\text{v00}.\text{fits} is the zeroth-order continuum component, \text{mytorus}\_\text{scattered}\_H\_500\_\text{v00}.\text{fits} accounts for the scattered continuum, and \text{mytl}\_V000010n\_Ep0000H500\_v00.\text{fits} models the fluorescent lines.

The MYTorus model can be used in two different configurations, named coupled and decoupled (Yaqoob 2012). We test both of them on our data, and we report the results in the following sections.

### 3.2.2. MYTorus in Coupled Configuration

In MYTorus, the angle between the axis of the torus and the line of sight, the so-called “torus inclination angle,” is a free parameter, which we hereafter define as \( \theta_{\text{obs}} \). The inclination angle varies in the range \( \theta_{\text{obs}} = 0^\circ - 90^\circ \), where \( \theta_{\text{obs}} = 0^\circ \) models a torus observed face-on and \( \theta_{\text{obs}} = 90^\circ \) is observed edge-on. In the coupled configuration, \( \theta_{\text{obs}} \) is set to be the same for all three MYTorus components.

We report in Table 2 the best-fit parameters obtained using the MYTorus coupled model. We fit the XMM-Newton data in the 0.6–10 keV energy range to avoid a known MYTorus fit issue below 0.6 keV, which may cause large statistical errors (more details are available in the MYTorus manual\(^7\)). The best-fit photon index is \( \Gamma = 1.52^{+0.17}_{-0.11} \) (the lower limit of the photon index cannot be constrained in our modeling since it falls below 1.4, the value that is the smallest value that can be tested with MYTorus). The photon index of the Compton-scattered continuum and of the iron emission feature component is set to be the same as that of direct continuum. The equatorial column density is \( N_{\text{H,eq}} = 3.02^{+0.25}_{-0.12} \times 10^{24} \text{ cm}^{-2} \). The inclination angle is \( \theta_{\text{obs}} = 62.53^{+4.38}_{-2.23}^\circ \), suggesting that we are observing through the brink of the torus. The line-of-sight column density is defined as \( N_{\text{H,obs}} = N_{\text{H,eq}} \left(1 - 4 \cos^2(\theta_{\text{obs}})\right)^{1/2} = 1.17^{+1.17}_{-1.07} \times 10^{24} \text{ cm}^{-2} \). The reduced \( \chi^2 \) is \( \chi^2_r = 231/239 = 0.97 \).

### 3.2.3. MYTorus in Decoupled Configuration

The decoupled MYTorus model, which is first introduced in Yaqoob (2012), adds flexibility to the MYTorus model, as it allows the users to model the absorber’s structure with a more general geometry and even simulate a clumpy distribution of the obscuring material. In this configuration, the direct continuum is a pure line-of-sight quantity, and the inclination angle of the direct continuum is fixed to \( \theta_{\text{obs,Z}} = 90^\circ \), such that the column density of the direct continuum models the line-of-sight column density, \( N_{\text{HZ}} \). The inclination angle of the Compton-scattered continuum and fluorescent lines is instead set to be either observed face-on, such that \( \theta_{\text{obs,S,L}} = 0^\circ \), or observed edge-on, i.e., \( \theta_{\text{obs,S,L}} = 90^\circ \). The face-on configuration mimics the reprocessed emission coming from the back side of the torus, which is expected to be more prominent in a patchy, less uniform torus, where the photons emitted by the back side of the torus have a smaller chance of being absorbed before reaching the observer. In the “edge-on” scenario, instead, the photons are reprocessed by the obscuring material lying between the AGN and the observer, and an edge-on-dominated reprocessed emission therefore favors a more uniform distribution of the obscuring material. In the decoupled MYTorus model, the column density of the scattered continuum and of the fluorescent lines, \( N_{\text{HS}} \), describes the “global average” column density of the torus, i.e., the average column density of the obscuring material, which can

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\(^7\) http://mytorus.com/mytorus-instructions.html
significantly differ from the line-of-sight value in an inhomogeneous, patchy torus.

In Yaqoob (2012), the decoupled \textsc{MYTorus} model is used adding to the model both the $\theta_{\text{obs,S.I}} = 90^\circ$ and the $\theta_{\text{obs,S.I.L}} = 0^\circ$ reprocessed components; thus, we first test this model, where both components contribute to the total reprocessed emission. In such a scenario, the best fit is $\chi^2/\text{dof} = 222/238 = 0.93$, while the intensity of the face-on component is 15 times smaller than the intensity of the “edge-on” component, suggesting that the reprocessed emission in NGC 1358 comes mostly from material located between the AGN and the observer. For this reason, following the approach described in Yaqoob et al. (2015), we refit our data twice, each time using only one of the two reprocessed component configurations. The best fit for the pure back-side reflection model, i.e., $\theta_{\text{obs,S.I}} = 0^\circ$, is presented in Table 2. The photon index is $\Gamma_{\text{LS}} = 1.66^{+0.15}_{-0.26}$, the line-of-sight column densities is $N_{\text{HZ,LS,S}=0} = 1.19^{+0.22}_{-0.27} \times 10^{24} \text{ cm}^{-2}$, and the “global average” column density is $N_{\text{HZ,LS,S}=0} = 5.25^{+2.86}_{-2.60} \times 10^{24} \text{ cm}^{-2}$. The best fit by using only $\theta_{\text{obs,S.I}} = 90^\circ$ is also presented in Table 2. The photon index is $\Gamma_{\text{LS}} = 1.85^{+0.13}_{-0.23}$. The line-of-sight column density is $N_{\text{HZ,LS,S}=90} = 2.40^{+0.40}_{-0.44} \times 10^{24} \text{ cm}^{-2}$. The “global average” column density is $N_{\text{HZ,LS,S}=90} = 0.50^{+0.12}_{-0.09} \times 10^{24} \text{ cm}^{-2}$. The “global average” column density is a few times smaller than the line-of-sight column density, suggesting a patchy torus scenario, where the AGN is observed through an overdense cloud.

In conclusion, the best fit of the decoupled \textsc{MYTorus} model in both face-on and “edge-on” configurations confirms the Compton-thick origin of NGC 1358 at the 3$\sigma$ confidence level. The \textsc{MYTorus} decoupled model in “edge-on” configuration produced the best fit, $\chi^2 = \chi^2/\text{dof} = 220/239 = 0.92$, and the most reasonable photon index ($\Gamma \sim 1.8$; see, e.g., Marchesi et al. 2016), among all the models and is thus our favorite model. Figure 2 shows the unfolded \textsc{NuSTAR} and \textsc{XMM-Newton} spectrum of NGC 1358, fitted with the decoupled \textsc{MYTorus} model in “edge-on” configuration.

### 3.2.4. \textit{borus02}

While \textsc{MYTorus} is known to be effective in modeling the X-ray spectra of heavily obscured AGNs, it assumes a fixed torus opening angle ($\theta_{\text{Tor}} = 60^\circ$, i.e., a covering factor $f_c = \cos \theta_{\text{Tor}} = 0.5$), limiting the model to a single torus geometry in coupled mode, and does not allow one to directly measure the covering factor even in the decoupled mode, although the latter can be in principle used to mimic different geometries of the obscuring material. To complement our analysis, we therefore fit the NGC 1358 spectrum using the recently published \textit{borus02} model (Baloković et al. 2018), an updated version of the so-called \textsc{BNtorus} model (Brightman & Nandra 2011). In \textit{borus02} the torus covering factor is a free parameter varying in the range of $f_c = 0.1-1$, corresponding to a torus opening angle $\theta_{\text{Tor}} = 0^\circ-84^\circ$.

\textit{borus02} is used in the following \textsc{xspec} configuration:

\begin{verbatim}
ModelID = constant * phabs * (borus02_v170323a.fits + zphabs * cabs * zpowerlw + constant2 * zpowerlw + mekal).
\end{verbatim}

Where \textit{borus02_v170323a.fits} is an additive table that models the reprocessed components, including the fluorescent line emission and the reprocessed continuum. The line-of-sight absorption is modeled by $zphabs \times cabs$ including Compton scattering lost out of the line of sight, which includes the effect of Compton scattering. The other components are similar to \textsc{MYTorus}.

The best-fit results are presented in Table 2. The photon index is $\Gamma = 1.79^{+0.13}_{-0.04}$. The line-of-sight column density is $N_{\text{HZ,Z,S}} = 2.40^{+0.39}_{-0.27} \times 10^{24} \text{ cm}^{-2}$, while the column density of the torus is $N_{\text{HZ,Z,S}} = 0.50^{+0.12}_{-0.09} \times 10^{24} \text{ cm}^{-2}$, which is in good agreement with the results of the \textsc{MYTorus} decoupled model in “edge-on” configuration. The covering factor of the torus is $f_c < 0.17$, i.e., a disk-like torus, which is strongly different from the setup of \textsc{MYTorus} model, which will be further discussed in Section 4. Finally, the angle between the torus axis and the observer line of sight is $\theta_{\text{obs}} > 86.8^\circ$, suggesting that the “edge-on” scenario is favored. Figure 3 shows the unfolded \textsc{XMM-Newton} and \textsc{NuSTAR} spectrum of NGC 1358, fitted by the \textit{borus02} model.

### 3.3. Summary of the Spectral Fit Results

Based on the fit statistic and on the reliability of the best-fit parameters, we believe that the decoupled \textsc{MYTorus} model in “edge-on” configuration is the best-fit model for NGC 1358. In our fits, all models have a good statistic, with $\chi^2_\nu \sim 0.9-1.1$; nonetheless, their physical interpretation varies significantly. For example, model B suggests a reflection-dominated scenario; in both the coupled \textsc{MYTorus} and decoupled \textsc{MYTorus} in face-on configuration, the Compton-scattered component contribution to the total observed emission is as significant as the direct continuum one; finally, the decoupled \textsc{MYTorus} in “edge-on” configuration, which gives the best statistic, suggests that the direct continuum dominates at $E > 10 \text{ keV}$ and the contribution of the reprocessed component...
is relatively smaller, and a similar result is also obtained using borus02.

We are going to use decoupled MYTorus in “edge-on” configuration as a reference in the rest of the paper because it allows one to compute the iron Kα line equivalent width, which cannot be done as straightforwardly using borus02, whose iron Kα line and the reprocessed component are coupled together. The only exception will be in Section 4.3, where the results of the borus02 model, in which \( f_c \) is a free parameter, will be used in discussing the torus covering factor; however, as mentioned above, the best-fit results of borus02 are in full agreement with those of the decoupled MYTorus in “edge-on” configuration.

3.4. Flux and Column Density Variability

While the majority of torus models, such as MYTorus and borus02, assume a uniform distribution of the obscuring material, several works in the past 25 years have shown that a clumpy distribution of optically thick clouds, the so-called “patchy torus,” is in fact a scenario favored by the observations (see, e.g., Krolik & Begelman 1988; Antonucci 1993; Jaffe et al. 2004; Elitzur & Shlosman 2006; Nenkova et al. 2008).

Mendoza-Castrejón et al. (2015) study the silicates’ spectral features at 10 and 18 \( \mu \)m in the mid-IR (MIR) band, showing that the distribution of the obscuring material around the SMBH has a clumpy structure. Following this scenario, it may be possible to observe changes of the line-of-sight column density, \( N_{\text{HIz}} \), with time. For this purpose, we divide our NuSTAR and XMM-Newton observations into three blocks: (i) The first one contains the 26 ks of NuSTAR observation taken before the beginning of the XMM-Newton observation. (ii) The second and third ones are obtained dividing the remaining 24 ks of NuSTAR data and the 48 ks XMM-Newton data into two even pieces, each one including 12 ks of NuSTAR observation and 24 ks of XMM-Newton observation. We remind that the NuSTAR observation was taken in blocks of \( \sim 3 \) ks each; therefore, the NuSTAR and XMM-Newton observations start at different times but finish at the same time. The background-subtracted NuSTAR FPMA and XMM-Newton MOS1 light curves of NGC 1358 are shown in Figures 4 and 5, respectively.

The three spectra are fitted with the phenomenological model, since we are mostly interested in measuring flux and/or column density variation. We report in Table 3 the best-fit \( \Gamma \), \( N_{\text{HIz}} \), and flux of 2–10 keV for each of the three subobservations. The flux and column density measured in the different blocks are consistent with each other, although those of block 1 are marginally offset with respect to the other two, a result that is mostly due to a calibration offset between XMM-Newton and NuSTAR. In fact, when fitting the block 2 and 3 NuSTAR data alone, we find a smaller discrepancy, and the results are in agreement at the 90% confidence level.

We also plot the contour of photon index and column density in Figure 6, where the red, green, and blue lines are at 68%, 90%, and 99% confidence levels, respectively. Time blocks 1–3 are plotted in solid, dashed, and dotted lines, respectively. As can be seen, both quantities are consistent among the three blocks, at a 90% confidence level.

Finally, we fit the NuSTAR 3–79 keV light curve (Figure 4) with a constant corresponding to the average count rate of our source, which is \( r = (2.3 \pm 0.3) \times 10^{-2} \) counts s\(^{-1}\). The best-fit statistic is \( \chi^2 = 9.3 \) and the fit has 10 dof. At the 99% confidence level, the light curve is strongly different from a constant if \( \chi^2 > 23.2 \). We repeat the above process for the 0.6–10 keV background-subtracted light curve of the XMM-Newton MOS1 module (Figure 5). The average count rate is \( r = (9.8 \pm 1.6) \times 10^{-3} \) counts s\(^{-1}\), and the best-fit statistic is \( \chi^2 = 19.0 \) with 9 dof. At the 99% confidence level, the light curve is strongly different from a constant if \( \chi^2 > 21.7 \).
Therefore, we find no obvious evidence of variability in either flux of absorbing column density.

### 3.5. Equivalent Width of the Iron Kα Line

Thanks to the excellent count statistics provided by NuSTAR and XMM-Newton in the 5–8 keV band, we were also able to place strong constraints on the Fe Kα line equivalent width (EW), a significant improvement with respect to Marchesi et al. (2017a), where only an upper limit on EW could be derived. We measure equivalent width EW_{pow} = 0.72^{+0.16}_{-0.10} keV and EW_{pex} = 0.63^{+0.15}_{-0.15} keV using model A and model B, respectively.

To measure the Fe Kα line EW with MYTorus, we use the approach described in Yaqoob et al. (2015). We therefore first measure the continuum flux, without including the emission line, at E_{Kα} = 6.4 keV. We then compute the flux of the fluorescent line component in the energy range E = 0.95E_{Kα}–1.05E_{Kα}, i.e., between 6.08 and 6.72 keV, rest frame. EW is then computed by multiplying by (1 + z) the ratio between the fluorescent line flux and the monochromatic continuum flux. We obtain EW_{coup} = 0.69^{+0.11}_{-0.13} keV, EW_{decoupl,θ=90} = 0.70^{+0.14}_{-0.14} keV, and EW_{decoupl,θ=0} = 0.65^{+0.13}_{-0.13} keV, such that all the MYTorus EW values are in good agreement with those obtained in the phenomenological model.

### 4. Discussion and Conclusions

#### 4.1. Compared with Previous Results

In this work, we report the results of the spectral analysis of quasi-simultaneous NuSTAR (50 ks) and XMM-Newton (48 ks) observations of NGC 1358, a nearby Seyfert 2 galaxy, which was recently found to be a CT-AGN candidate (Marchesi et al. 2017a) based on its combined Swift-BAT and Chandra spectrum. The limited quality of the Chandra and Swift-BAT spectra was reflected in the rather large (~30%-40%) 90% confidence parameter uncertainties, and NGC 1358 Compton thickness could not be validated beyond the 1σ confidence level. More in detail, Marchesi et al. (2017a) used MYTorus coupled configuration to model the combined Chandra–Swift-BAT spectrum of NGC 1358. Their best fit ($\chi^2$/dof = 14.8/13) gave a column density of $N_{H,z} = 1.05^{+0.42}_{-0.36} \times 10^{24}$ cm$^{-2}$ assuming an inclination angle of $\theta_{\text{obs}} = 90°$. NGC 1358 was first reported as a candidate CT-AGN by Marinucci et al. (2012), which measured the X-ray spectral properties of NGC 1358 by fitting a 2–10 keV XMM-Newton spectrum observed in 2005 (exposure time 12.7 ks) with a Compton reflection model (pexray). The column density they obtained is $N_{H,z} = 1.30^{+0.50}_{-0.60} \times 10^{24}$ cm$^{-2}$, in good agreement with the findings of Marchesi et al. (2017a). Once again, the CT nature of NGC 1358 was not confirmed at a >$1\sigma$ significance level.

The first main result of our analysis is therefore that NGC 1358 is a confirmed, bona fide Compton-thick AGN, based on the two models that provide the most reliable fit, i.e., the decoupled MYTorus model in “edge-on” configuration and the borus02 model. More in detail, our best-fit line-of-sight column density obtained by the MYTorus decoupled model in “edge-on” configuration is $N_{H,z} = 2.40^{+0.40}_{-0.44} \times 10^{24}$ cm$^{-2}$, and for most of the parameters, the uncertainties are <20% at 90% confidence.

#### 4.2. Intrinsic X-Ray Luminosity

In Table 2, we report the observed flux and intrinsic luminosity of NGC 1358 in the 2–10 keV and 10–40 keV energy ranges, for all the different models discussed in Section 3. The observed flux values are consistent among both the phenomenological and the physical models, in both energy ranges. We instead observe significant differences between the best-fit luminosity values, since the decoupled MYTorus model in “edge-on” configuration and the borus02 model give a 2–10 keV intrinsic luminosity $L_{2–10\text{ keV}} \sim 2.06 \times 10^{43}$ erg s$^{-1}$, while the intrinsic luminosity in 2–10 keV for the other models is $L_{2–10\text{ keV}} < 0.4 \times 10^{43}$ erg s$^{-1}$, which is at least 6 times smaller than the best-fit models. This large difference is a direct consequence of the fitted results: in the phenomenological models, the coupled MYTorus model and the decoupled MYTorus face-on model, NGC 1358 is intrinsically less luminous, has a harder (somewhat unphysical, particularly in the phenomenological model) photon index, is less obscured, and has a strong reprocessed component. In the decoupled MYTorus “edge-on” model and in borus02, instead, NGC 1358 is more luminous, is more obscured, has a softer, more typical photon index, and the reprocessed component is relatively small.

Moreover, the intrinsic X-ray luminosity can also be inferred from luminosities derived at different wavelengths, e.g., the MIR luminosity (see, e.g., Elvis et al. 1978) and the [OIII] luminosity (see, e.g., Heckman et al. 2005). The MIR luminosity of NGC 1358 is obtained by using the flux at 12 μm, $L_{12\text{ μm}} = (1.43 \pm 0.03) \times 10^{-2}$ Jy (Wright et al. 2010); the corresponding luminosity is $L_{12\text{ μm}} = (1.23 \pm 0.03) \times 10^{22}$ erg s$^{-1}$. Using the $L_{\text{MIR}}$–$L_{2–10\text{ keV}}$ relation in Asmus et al. (2015), we then obtain the MIR-inferred X-ray intrinsic luminosity $L_{2–10\text{ keV},\text{MIR}} \sim 5.2 \times 10^{41}$ erg s$^{-1}$. The [OIII] luminosity of NGC 1358 is reported in Whittle (1992) and is $L_{\text{[OIII]}} = 9.8 \times 10^{40}$ erg s$^{-1}$. Applying the $L_{\text{[OIII]}}$–$L_{2–10\text{ keV}}$ relation from Georgantopoulos & Akylas (2010), we obtain the [OIII]-inferred X-ray intrinsic luminosity $L_{2–10\text{ keV},\text{[OIII]}} \sim 5.31 \times 10^{42}$ erg s$^{-1}$. Notably, these luminosities are in better agreement with those computed using the phenomenological models, the coupled MYTorus model and the decoupled MYTorus model in face-on configuration, rather than with that derived using the decoupled, edge-on MYTorus.
model that we selected as our best-fit model. However, we point out that both $L_{\text{MIR}}-L_{2-10\text{ keV}}$ and the $L_{\text{bol}}-L_{2-10\text{ keV}}$ relations are derived using phenomenological models, which are known to be less reliable than the physical models when fitting the heavily obscured AGNs, such as NGC 1358. The low MIR luminosity reported above may be due to the low covering factor of the torus in NGC 1358 (see the next section). However, despite being disfavored by the data, the possibility that the source is less obscured and intrinsically fainter than suggested by the best-fit model cannot be ruled out.

4.3. Covering Factor

One of the advantages in fitting the X-ray spectra of heavily obscured AGNs using a physical model is the possibility to measure specific torus parameters, such as the torus covering factor, $f_c$. In borus02 the covering factor is a free parameter: we find that the best-fit borus02 solution supports a low-$f_c$ scenario for NGC 1358, with $f_c < 0.17$, thus suggesting a “disk-like” torus. Such evidence is supported also by the MYTorus best-fit model; in fact, while in MYTorus $f_c$ is not a free parameter, the ratio between the normalization of the intrinsic continuum and the one of the Compton-scattered continuum, $A_P$, can be used as a proxy of the torus covering factor. More in detail, from our best-fit MYTorus model, i.e., the decoupled edge-on one, we obtain $A_S = 0.23^{+0.18}_{-0.06}$. The estimated covering factor is then $f_c = 0.5 \times A_S = 0.12^{+0.09}_{-0.03}$, again supporting a “disk-like” torus scenario. However, it is worth mentioning that Yaqoob (2012) points out that the existence of a non-negligible time delay between the two components can also result in the relative normalization being away from unity.

Finally, we checked for further evidence of a “disk-like” torus scenario using the ratio of the torus luminosity to the AGN luminosity as a proxy of the torus covering factor (Stalevski et al. 2016). We indirectly infer the torus luminosity from the 12 $\mu$m luminosity, which is dominated by the emission reprocessed by the torus. We can then derive a first-order estimate of the dust torus covering factor, $f_t = L_{\text{tor}}/L_{\text{bol}} \sim 0.005$, where $L_{\text{tor}}$ is the torus luminosity and $L_{\text{bol}} = 2.34 \times 10^{44}$ erg s$^{-1}$ (Woo & Urry 2002) is the bolometric luminosity of the AGN. While this result needs to be validated by a more accurate modeling and fit of the torus SED, it still points to a “disk-like” torus scenario.

4.4. Clumpiness of the Torus

In Section 3.2, we computed both the line-of-sight column density, $N_{\text{H,LS}}$, and the torus “global average” column density, $N_{\text{H,TZ}}$, using both MYTorus in its decoupled configuration and borus02. In both cases, we find a mild (~4 times) difference between the line-of-sight column density and the torus “global average” column density, evidence that supports an inhomogeneous distribution of the obscuring material surrounding the accreting SMBH in NGC 1358. We point out that this statement may seem in contradiction with what we stated in Section 3.2.3 when presenting the MYTorus decoupled face-on model, i.e., the fact that the face-on model, rather than the “edge-on” one, should be more effective in characterizing a patchy torus scenario, where there is a higher chance to observe the reprocessed emission coming from the back side of the torus. However, this potential discrepancy can be explained assuming that in NGC 1358 the torus covering factor is indeed small, and the reprocessed component contribution to the overall observed emission is therefore small; consequently, since the back-side reprocessed component is expected to be a fraction of the front-side one, in this specific case it is basically negligible.

To further investigate this potential “patchy torus” scenario, in Section 3.4 we divide our NuSTAR and XMM-Newton observations into three blocks and fit each of the subobservations. As can be seen in Table 3, all the parameters are in agreement within the uncertainties, and no variability is therefore detected. This suggests that the timescale associated with a significant positional change of the clouds within the
torus is much larger than $\sim 50$ ks or that the torus is more uniformly distributed than what the best-fit model suggests. However, the lack of significant variability in a 50 ks observation provides us with a way to set a lower limit on the size of obscuring clouds. Assuming that the obscuring clouds are $r = 1$ pc away from the accreting SMBH (see, e.g., Almeida & Ricci 2017), the mass of the supermassive black hole in NGC 1358 is $M_{BH} = 7.88$ (Woo & Urry 2002), such that the velocity of the clouds is $v_{cloud} = (GM_{BH}/r)^{1/2} = 570$ km s$^{-1}$, which is in line with the FWHM velocity obtained from the velocity broadening of the emission lines. Therefore, the lower limit to the radius of the obscuring cloud should be $R_{cloud} = v_{cloud} \times 50$ ks $= 3 \times 10^7$ km $\sim 43 R_{\odot}$.

4.5. Eddington Ratio and Mass Accretion Rate

Finally, we analyzed our X-ray data to derive the Eddington ratio and mass accretion rate of the SMBH in NGC 1358. The Eddington ratio is a measurement of the SMBH accretion efficiency and is defined as $\lambda_{Edd} = L_{bol}/L_{Edd}$, i.e., as the ratio between the bolometric luminosity, $L_{bol}$, and the so-called Eddington luminosity, $L_{Edd} = 4\pi GM_{BH}m_{p}/c^{2}$, where $M_{BH}$ is the SMBH mass and $m_{p}$ is the mass of proton.

Woo & Urry (2002) report a measurement of both the black hole mass and the bolometric luminosity of NGC 1358. The mass of the black hole is obtained by the correlation between the black hole mass and stellar velocity dispersion, and the bolometric luminosity is obtained through direct integration of the spectral energy distribution. Based on these values, the Eddington ratio of NGC 1358 is $\lambda_{Edd} = 2.5 \times 10^{-2}$.

Our high-quality X-ray data allow us to recompute $L_{bol}$, extrapolating it from our best-fit 2–10 keV intrinsic luminosity, $L_{bol,2-10\text{ keV}} = 2.06_{-0.11}^{+0.11} \times 10^{43}$ erg s$^{-1}$. We use the bolometric correction of Marconi et al. (2004, Equation (21)), finding a bolometric luminosity $L_{bol} = 4.36_{-0.30}^{+0.29} \times 10^{44}$ erg s$^{-1}$. Thus, the corresponding Eddington efficiency is $\lambda_{Edd} \approx 4.7_{-0.3}^{+0.3} \times 10^{-2}$, which is typical for AGNs in the range of 0.001–1, using the black hole mass value from Woo & Urry (2002). This result is also consistent with Marinucci et al. (2012), which reported an Eddington ratio of $\lambda_{Edd} \approx 1.62 \times 10^{-2}$, relying on an estimate of the black hole mass of log($M_{BH}/M_{\odot}$) $= 7.99$ and a bolometric luminosity $L_{bol} = 2.04 \times 10^{44}$ erg s$^{-1}$.

Schönherr-Müller et al. (2017) estimated an NGC 1358 ionized mass inflow rate (excluding the neutral and molecular gas, being only the lower limit of the total mass inflow) of $M_{in} \approx 1.5 \times 10^{-2} M_{\odot}$ yr$^{-1}$ in the inner 180 pc. The authors also report a mass accretion rate, obtained using the [O III] luminosity from Gu & Huang (2002) and the bolometric correction from Lamastra et al. (2009), of $\dot{m}_{acc} \sim 0.9 \times 10^{-4} M_{\odot}$ yr$^{-1}$, which is 160 times smaller than the mass inflow rate of NGC 1358. According to the relationship between the mass accretion rate and the bolometric luminosity, $\dot{m}_{acc} = L_{bol}/\eta c^{2}$, where $\eta$ is the efficiency that converts the rest-mass energy of accreted material into radiation and is assumed to be $\eta = 0.1$ (Frank et al. 2002), we also estimate the mass accretion rate in NGC 1358, which is $\dot{m}_{acc} = (7.2-8.2) \times 10^{-2} M_{\odot}$ yr$^{-1}$ adopting the bolometric luminosity from our best fit, which is in the same order as the mass inflow rate reported in Schönherr-Müller et al. (2017); the large difference between the mass accretion rate and the mass inflow rate reported in Schönherr-Müller et al. (2017) could be diminished when the bolometric luminosity is measured from the 2–10 keV X-ray band rather than from the [O III] luminosity.

As shown here, NuSTAR and XMM-Newton are instrumental to identify and study CT-AGNs in detail. We envision that extending these studies to most CT-AGNs known in the local universe will allow us to shed light on the (so far elusive) population of CT-AGNs.

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**References**

Ajello, M., Greiner, J., Sato, G., et al. 2008, ApJ, 689, 666
Alexander, D. M., Bauer, F. E., Brandt, W. N., et al. 2003, AJ, 126, 539
Almeida, C. R., & Ricci, C. 2017, NatAs, 1, 679
Anders, E., & Grevesse, N. 1989, GeCoA, 53, 197
Annunziatell, A., Dietrich, D. M., Gandhi, P., et al. 2017, ApJ, 836, 165
Annunziatell, A., Gandhi, P., Alexander, D. M., et al. 2015, ApJ, 815, 36
Antonucci, R. 1993, ARA&A, 31, 473
Arnaud, K. A. 1996, in ASP Conf. Ser. 101, Astronomical Data Analysis Software and Systems V, ed. G. H. Jacoby & J. Barnes (San Francisco, CA: ASP), 17
Asmus, D., Gandhi, P., Hönig, S. F., Snette, A., & Duschl, W. J. 2015, MNRAS, 454, 766
Baloković, M., Brightman, M., Harrison, F. A., et al. 2018, ApJ, 854, 42
Baloković, M., Comastri, A., Harrison, F. A., et al. 2014, ApJ, 794, 111
Barthelmy, S. D., Brandt, W. L., Cummings, J. R., et al. 2005, SSRT, 120, 143
Bauer, F. E., Arévalo, P., Walton, D. J., et al. 2015, ApJ, 812, 116
Boller, T., Freyberg, M. J., Trümper, J., et al. 2016, A&A, 598, A103
Buchner, J., Georgakakis, A., Nandra, K., et al. 2011, MNRAS, 413, 1206
Burlon, D., Ajello, M., Greiner, J., et al. 2011, ApJ, 728, 58
Elitzur, M., & Shlosman I. 2006, ApJL, 648, L101
Elvis, M., Maccacaro, T., Wilson, A. S., et al. 1978, MNRAS, 183, 129
Frank, J., King, A., & Raine, D. J. 2002, Accretion Power in Astrophysics (3rd ed.; Cambridge: Cambridge Univ. Press)
Furui, S., Fukushima, Y., Oda, H., et al. 2016, ApJ, 818, 164
Gandhi, P., & Fabian, A. C. 2003, MNRAS, 339, 1095
Georgantopoulos, I., & Akylas, A. 2010, A&A, 510, 906
Georgantopoulos, I., Comastri, A., Vignali, C., et al. 2013, A&A, 555, A43
Gilli, R., Comastri, A., & Hasinger, G. 2007, A&A, 463, 79
Gu, Q., & Huang, J. 2002, ApJ, 579, 205
Harrison, F. A., Craig, W. W., Christensen, F. E., et al. 2013, ApJ, 770, 103
Heckman, T. M., Ptak, A., Hornschemeier, A., & Kauffmann, G. 2005, ApJ, 634, 161
Ikeda, S., Awaki, H., & Terashima, Y. 2009, ApJ, 692, 608
Jaffe, W., Meisenheimer, K., Röttgering, H. J. A., et al. 2004, Natur, 429, 47, EP
Jansen, F., Lumb, D., Altieri, B., et al. 2001, A&A, 365, L1
Kalberla, P. M. W., Burton, W. B., Hartmann, D., et al. 2005, A&A, 440, 775
Koss, M. J., Assef, R., Baloković, M., et al. 2016, ApJ, 825, 85
Krolik, J. H., & Begelman, M. C. 1988, ApJ, 329, 702
Lamastra, A., Bianchi, S., Matt, G., et al. 2009, A&A, 504, 73
Lanzuisi, G., Ranalli, P., Georgantopoulos, I., et al. 2015, A&A, 573, A137
Liu, Y., & Li, X. 2014, ApJ, 787, 52
Magdziarz, P., & Zdziarski, A. A. 1995, MNRAS, 273, 837
Marchesi, S., Ajello, M., Comastri, A., et al. 2017a, ApJ, 836, 116
Marchesi, S., Ajello, M., Marcotulli, L., et al. 2018, ApJ, 854, 49
Marchesi, S., Lanzuisi, G., Civano, F., et al. 2016, ApJ, 830, 100
Marchesi, S., Tremblay, L., Ajello, M., et al. 2017b, ApJ, 848, 53
Marconi, A., Risaliti, G., Gilli, R., et al. 2004, MNRAS, 351, 169
Marinucci, A., Bianchi, S., Nicastro, F., Matt, G., & Goulding, A. D. 2012, ApJ, 748, 130
Matt, G., & Fabian, A. C. 1994, MNRAS, 267, 187
Mendoza-Castrejón, S., Dultzin, D., Krongold, Y., González, J. J., & Elitzur, M. 2015, MNRAS, 447, 2437
Mewe, R., Gronenschild, E. H. B. M., & van den Oord, G. H. J. 1985, A&AS, 62, 197
Murphy, K. D., & Yaqoob, T. 2009, MNRAS, 397, 1549

Nenkova, M., Sirocky, M. M., Ivezić, Ž., & Elitzur, M. 2008, ApJ, 685, 147
Puccetti, S., Comastri, A., Fiore, F., et al. 2014, ApJ, 793, 26
Ricci, C., Ueda, Y., Koss, M. J., et al. 2015, ApJL, 815, L13
Ricci, C., Walter, R., Courvoisier, T. J.-L., & Paltani, S. 2011, A&A, 532, A102
Risaliti, G., Maiolino, R., & Salvati, M. 1999, ApJ, 522, 110
Schnorr-Müller, A., Storchi-Bergmann, T., Nagar, N. M., Robinson, A., & Lena, D. 2017, MNRAS, 471, 3888
Stalevski, M., Ricci, C., Ueda, Y., et al. 2016, MNRAS, 458, 2288
Theureau, G., Bottinelli, L., Coudreau-Durand, N., et al. 1998, A&AS, 130, 333
Treister, E., Urry, C. M., & Virani, S. 2009, ApJ, 696, 110
Ueda, Y., Akikiyama, M., Hasinger, G., Miyaji, T., & Watson, M. G. 2014, ApJ, 786, 104
Ursini, F., Bassani, L., Panessa, F., et al. 2018, MNRAS, 474, 5684
Verner, D., Ferland, G., Korista, K., & Yakovlev, D. 1996, ApJ, 465, 487
Whittle, M. 1992, ApJS, 79, 49
Winkler, C., Courvoisier, T. J.-L., Di Cocco, G., et al. 2003, A&A, 411, L1
Woo, J.-H., & Urry, C. M. 2002, ApJ, 579, 530
Wright, E. L., Eisenhardt, P. R. M., Mainzer, A. K., et al. 2010, AJ, 140, 1868
Yaqoob, T. 2012, MNRAS, 423, 3360
Yaqoob, T., Tatum, M. M., Scholtes, A., Gottlieb, A., & Turner, T. J. 2015, MNRAS, 454, 973