Density determinations in heavy ion collisions

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The experimental determination of freeze-out temperatures and densities from the yields of light elements emitted in heavy ion collisions is discussed. Results from different experimental approaches are compared with those of model calculations carried out with and without the inclusion of medium effects. Medium effects become of relevance for baryon densities above ≈ 5 × 10−4 fm−3. A quantum statistical (QS) model incorporating medium effects is in good agreement with the experimentally derived results at higher densities. A densitometer based on calculated chemical equilibrium constants is proposed.

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Heavy ion collisions (HIC) are often used as a tool to investigate the properties of excited nuclear matter. Measured yields of different ejectiles as well as their energy spectra and their correlations in momentum space can be used to infer the properties of the emitting source. Despite the fact that a great deal of experimental data has been accumulated from HIC during the last few decades, reconstruction of the properties of the hot expanding nuclear system remains a difficult task. Two major problems are the complications inherent in incorporating non-equilibrium effects and in the treatment of strong correlations that are already present in equilibrated nuclear matter.

An often employed simple approach to handling these effects is the freeze-out approximation. Starting from hot dense matter produced in HIC, this approach assumes the attainment of local thermodynamic equilibrium after a short relaxation time. Chemical equilibrium may also be established in the expanding fireball if the collision rates in the expanding hot and dense nuclear system are above a critical value.

While more microscopic approaches employing transport models that describe the dynamical evolution of the many particle system are being pursued, a freeze-out approach provides a very efficient means to get a general overview of the reaction. Such approaches have been applied in heavy-ion reactions, to analyze the equation of state of nuclear matter, see [1], but also recently in high-energy experiments (RHIC, LHC) to describe the abundances of emitted elementary particles [2]. Much information on the symmetry energy, on phase instability, etc., has been obtained using this concept.

Within the freeze-out approximation, the abundances of emitted particles and clusters at freeze-out are determined by the temperature T, the baryon density n_B, and the isospin asymmetry δ = (n_n − n_p)/n_B, which is related to the total proton fraction Y_p = (1 − δ)/2. In this paper we discuss the extraction of densities and temperatures from the measured yields of ejectiles in HIC. We focus on the information content of neutrons (n), protons (p), deuterons (d), tritons (t), 3He (h), and 4He (α) particles, emitted in near Fermi energy reactions. To extract the relevant information we optimize the freeze-out approach by including correlations and density effects using systematic, consistent quantum statistical approaches.

We are considering only the yields Y_i of these particles, the energy spectra are established by long-range interactions and will not be discussed here. It is possible to extend the approach also to other situations where not only particles with A ≤ 4 are of relevance. Whereas the asymmetry is easily obtained from the proton and neutron number of all emitted fragments, for the determination of the temperature many efforts have been made. In particular, double ratios have been considered. We will not discuss these results here. In contrast, the determination of the density is a serious problem that has not been solved in a satisfactory manner until now. We will give the reason and propose a solution of this problem.

Experiments and Data Analysis Using the Nuclear Statistical Equilibrium (NSE). The NIMROD collaboration has recently measured yields of light particles in three different experiments performed at energies near the Fermi energy. Collisions of 64Zn projectiles with 92Mo and 197Au target nuclei [3] and the collisions 70Zn+70Zn, 64Zn+64Zn, and 64Ni+64Ni were studied at E/A = 35 MeV/nucleon [4]. Collisions of 40Ar + 112Sn, 124Sn and 64Zn + 112Sn, 124Sn [5] were studied at 47 MeV/nucleon. These experiments have been described in several papers [3, 5, 8] where the details are given.

Our goal is to derive T, n_B, and δ from the five experimental yields, Y_p, Y_d, Y_t, Y_h, Y_α, of the light charged Z = 1, 2 species (The neutron yields are not accurately measured but, under equilibrium assumptions, can be ascertained from the proton yields combined with t/h ratios as indicated below.) This problem is easily solved in the low-density limit where the NSE can be applied,

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i.e. below \( n_B \approx 10^{-4} \text{ fm}^{-3} \) and at moderate temperatures where medium effects can be neglected. Using the simple relations for the non-degenerate ideal mixture of reacting components

\[
n_i = \frac{2s_i + 1}{A_i^2} e^{(E_i + Z_i \mu_p + N_i \mu_n)/T},
\]

where \( A_i^2 = 2\pi h^2/(m_i T) \) denotes the thermal wave length, \( m_i \) the mass, \( s_i \) the spin, and \( E_i \) the binding energy of the different components, one can construct expressions that are almost directly related to the different thermodynamic parameters.

In particular the ratio \( Y_n/Y_t \) can be used to determine the asymmetry of the nuclear system. It can also be used to give an estimate of the neutron yield

\[
Y_n = Y_p \frac{Y_t}{Y_p} f_\delta(T)
\]

where \( f_\delta(T) = \exp[(E_{4\text{He}} - E_t)/T][(m_n m_k)/(m_p m_k)]^{3/2} \) is a correction that accounts for the difference in the binding energies of \( ^3\text{H} \) and \( ^4\text{He} \). For the sake of simplicity we use in the following the approximation \( m_A = Am \) with the average baryon mass, \( m \).

The temperature can be determined by a double ratio of yields chosen so that the chemical potentials are almost directly related to the different excitation energies of the different components, one can construct expressions to derive in-medium few-body wave equations, see \[11\]. Comparing to the zeroth order NSE, improvements are obtained, in particular:

i) The classical Boltzmann distribution is replaced by the Fermi or Bose distributions if degenerate effects are to be accounted for. This follows immediately from a quantum statistical approach. In a similar spirit, the momentum quadrupole and normalized number fluctuations for light particle emission in HIC have been analyzed in Ref. \[8\]. In that work it has been proposed to use the reduction of fluctuations for Fermi systems or enhancement of fluctuations for Bose systems to estimate the thermodynamic parameters.

ii) With increasing density, medium effects have to be included. Within a quasiparticle picture, the binding energies of the bound states are decreasing with increasing density due to Pauli blocking. Depending on temperature and center of mass momentum, the bound states merge in the continuum at the so-called Mott density.

iii) In a QS approach, contributions of the continuum to the density also arise (scattering states). Within a

\[
R_{\text{test}} = 4^\epsilon \left( \frac{27}{16} \right)^{3/2} \left( \frac{3}{4} \right) \left( \frac{8}{9} \right)^{3/2} \frac{Y_{4\text{He}}^{2\epsilon - 1} Y_p^{\epsilon - 1}}{Y_t^{2\epsilon - 1} Y_{4\text{He}}^{\epsilon - 1}},
\]

with \( \epsilon = (E_\alpha + E_d - E_t - E_{4\text{He}})/(2E_\alpha - E_t - 2E_{4\text{He}}) = 0.43833 \), the prefactor of the yield fraction has the value 1.62796.

From NSE follows \( R_{\text{test}} \approx 1 \). This quantity is also easily determined from measured yields. In particular, the data obtained in the experiment Ref. \[3\] give in total summed over \( v_s \) \( R_{\text{test}} = 1.22 \), the data of \[5\] lead to \( R_{\text{test}} = 1.36 \), and the data of \[8\] to 1.147 (summed over all excitation energies). Apparently, in comparison with the yields of bound nucleons, the yield \( Y_p \) is higher than expected within NSE.

Different reasons can be given for this deviation:

i) The assumption of thermodynamic equilibrium is not realized. One has to investigate the dynamical non-equilibrium expansion of the fireball produced in HIC.

ii) The source is more complex.

iii) The assumption of an ideal mixture of colliding, but otherwise non-interacting components (free nucleons and clusters) must be improved.

We will not discuss how the freeze-out concept has to be modified when non-equilibrium and finite size effects are taken into account. Rather here we focus on the last point - improving the approximation of an ideal mixture by considering effects of correlations in the medium. This can be done within a systematic quantum statistical approach.

**Quantum statistical (QS) approach**. Within a quantum statistical approach to nuclear matter, correlations and bound state formation are treated using Green’s functions to derive in-medium few-body wave equations, see \[11\]. Comparing to the zeroth order NSE, improvements are obtained, in particular:

i) The classical Boltzmann distribution is replaced by the Fermi or Bose distributions if degenerate effects are to be accounted for. This follows immediately from a quantum statistical approach. In a similar spirit, the momentum quadrupole and normalized number fluctuations for light particle emission in HIC have been analyzed in Ref. \[8\]. In that work it has been proposed to use the reduction of fluctuations for Fermi systems or enhancement of fluctuations for Bose systems to estimate the thermodynamic parameters.

ii) With increasing density, medium effects have to be included. Within a quasiparticle picture, the binding energies of the bound states are decreasing with increasing density due to Pauli blocking. Depending on temperature and center of mass momentum, the bound states merge in the continuum at the so-called Mott density.

Since the composition is determined by the quasiparticle energies, the cluster abundances are suppressed. As a consequence, the mass fraction of free nucleons is enhanced compared with the NSE, as shown in the following. (See also Ref. \[10\].)

iii) In a QS approach, contributions of the continuum to the density also arise (scattering states). Within a
virial expansion, for each channel where a bound state is formed, scattering states will also contribute to the equation of state. An upper limit for the contributions of the continuum can be given subtracting for each bound state the same term with zero binding energy. These continuum contributions are small in the region considered here and are neglected in the present work. Future investigations are needed to account the continuum correlations.

Because the ratio of free nucleons to bound clusters is strongly influenced by medium effects the use of the NSE is limited to very small densities. Compared to the NSE, in the QS approach the concentration of bound states is going down, whereas the fraction of free nucleons increases. This modifies the yield fractions that contain the free nucleon yields.

**Temperature Determinations in Low Density Nuclear Matter.** At densities below the Mott point the effect of medium modifications on the double isotope ratios is not strong [10]. Thus, to a good approximation the determination of the temperature can be performed employing the double ratios, Eq. (3). In Refs. [4][5][7] this technique is employed to characterize the temperature evolution of the expanding nascent fireball (the intermediate velocity or nucleon-nucleon source) by associating particle velocity with emission time. (The Albergo expression, Eq. (3), is modified by a factor $(9/8)^{1/2}$ in front of the double ratio when applied to particles with the same surface velocity, see [3].) In Ref. [8] which focuses on quasiprojectile sources of different excitation energy, temperatures have been calculated employing the momentum quadrupole fluctuation method. In the comparisons which follow, the temperatures are those derived in the quoted references.

**Density Determinations.** The main problem is the determination of the density because the influence of medium effects can be strong. In the following we compare results from four different approaches to determination of the density, i) the Albergo NSE based relations [3], ii) the Mekjian coalescence model which takes into account three body terms which might mimic either a higher density (three body collisions) or Pauli blocking, iii) the quantum fluctuation analysis method [8], and iv) an approach based on use of the Chemical equilibrium constant employed in Refs. [5][7]. The use of the first three of these techniques to extract temperatures and densities have been well described in the references cited. The use of the chemical equilibrium constant, introduced in [5], to characterize the relative yields

$$K_c(A, Z) = \frac{\rho(A, Z)}{n_B^2 n_Z}.$$

has some particular advantages. In contrast to the free proton fraction, these chemical equilibierum constants, while sensitive to the effects of the medium, are not dependent on the asymmetry parameter or the choice of competing species present in a model in the low-density limit where the NSE can be applied. Specifically, to infer the values for the thermodynamic parameters of nuclear matter in HIC at freeze-out from experimental data we define the quantity $\tilde{K}_c$ that is related to the chemical equilibrium constant for $\alpha$ particle formation and can be directly determined from the observed experimental yields,

$$\tilde{K}_c = \frac{Y_A Y_Z^2}{Y_p Y_t^2} \left( \sum_i A_i Y_i \right)^3 = \frac{n_{A,Z}}{n_p^{n_d} n_t}. \quad (8)$$

The second relation is found by dividing the particle numbers by their common volume. This modified chemical constant $\tilde{K}_c$ does not depend on the volume of the system. Note that the baryon density equals $n_B = n_p + n_n + 2n_d + 3n_t + 3n_h + 4n_\alpha$, if the ejectiles are restricted to $A \leq 4$. In general, clusters with higher $A$ must included if they are formed from the source under consideration.

Within NSE we can show that

$$\ln K_{c,NSE} = 3 \ln n_B + f_\alpha(T). \quad (9)$$

Is applicable for the low-density region, $f_\alpha(T) = (E_\alpha + 2E_h - 2E_\beta)/T + (9/2) \ln[2\pi \hbar^2/(mT)] - \ln 2$. The quasiparticle shifts we have previously calculated for the single nucleons as well as for the light clusters [11], indicate that medium effects are relevant above the density of about $n_B = 5 \times 10^{-4} \text{fm}^{-3}$. In Figure 2 we present theoretical values of $\tilde{K}_c$ which have been calculated assuming including QS corrections (symmetric matter). The decrease of $\tilde{K}_c$ for densities above $10^{-2} \text{fm}^{-3}$ is due to the Mott effect that bound states disapper because of Pauli blocking, see [9].
In our calculations we find essentially no dependence on the asymmetry parameter as should be expected for the chemical equilibrium expression. In principle this plot constitutes a densitometer which may be employed to estimate the density from experimental yields if the temperature has been determined. However, in general there are two solutions so that one has to select out the correct one. For comparison to the theoretical values presented in Figure 2 we present also in that figure experimental yields (thin dotted lines) and QS calculations (bold straight lines).

FIG. 2: (Color online) Chemical constant $\tilde{K}_h$ as function of density and temperature. Data (stars) for $T = 5, 6, 7, 8, 9, 10, 11$ MeV are compared with the NSE values (thick dotted lines) and QS calculations (bold straight lines).

Discussion. Substantial progress has been made in the effort to explore nuclear matter at subsaturation densities. There is now experimental evidence that proves the relevance of incorporating medium effects such as Pauli blocking and the Mott effect into theoretical treatments. As expected from a quantum statistical approach, the NSE based on non-interacting components is not sufficient to explain the data from experiments that investigate nuclear systems at densities around one tenth of saturation density and above. Considering the clusters as quasiparticles, a smooth transition from the NSE at low densities to mean-field approaches at the saturation density can be modeled \cite{14}. The Albergo densitometer is restricted to very low densities. The densitometer proposed here, based upon chemical equilibrium constants calculated within the framework of the QS model, can be applied at significantly higher densities.

According to Fig. 2, measured yields of light elements can be used to infer the baryon density if the temperature is known. Despite the double valued solution, this diagram may serve as an important tool to derive densities from measured yields. Two other independent methods have been used to infer densities from the yields of light clusters:

i) The Mekjian coalescence model \cite{12} has been used. Coalescence parameters $P_0$ were calculated for the different clusters, see \cite{7}, and used to determine volumes. The corresponding volume was used to convert the measured yields into densities. The results are shown in Figs. 2 and 3.

ii) An alternative approach to infer the parameter values for density and temperature, proposed in \cite{8}, employs quadrupole momentum fluctuations and the fluctuations of fermion and boson numbers in the nuclear system. Compared with classical systems number fluctuations are decreased for fermion systems and increased for boson systems if the temperature approaches the critical temperature.

FIG. 3: (Color online) Baryon density derived from yields of light elements. Data according to \cite{3, 5, 8} are compared with the results of the analysis of yields using NSE and QS calculations for $\tilde{K}_h$. 

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The density values derived by both the coalescence and fluctuation methods in rather good agreement with QS results that include medium effects, but in disagreement with the values derived from NSE. Only below densities of about $5 \times 10^{-4}$ fm$^{-3}$, the NSE is applicable.

The discrepancies with NSE are substantially reduced if medium effects such as Pauli blocking [11] or, alternatively, excluded volume [12, 15] are taken into account. The fact that the two different experimental results for the temperature and density regions explored are consistent with each other despite the fact that they are obtained from quite different emitting sources and analyses, suggests that an underlying unifying feature of the EOS is responsible. Indeed, further analysis by Mabiala et al. [8] indicate that the data are sampling the vapor branch of the liquid gas coexistence curve and within the framework of the Guggenheim systematics may be employed to determine the critical temperatures of mesoscopic nuclear systems, in a manner analogous to previous treatments [16, 17].

In conclusion we note some open questions with respect to the present determination of thermodynamic parameter values:

i) The formation of larger clusters is neglected. For their inclusion see Ref. [15]. The chemical equilibrium constants are not sensitive to the formation of other clusters.

ii) Continuum correlations are not taken into account. Possibly they are less important if the quasiparticle picture and resonances for nearly bound states are included. A non-equilibrium approach is needed to follow continuum correlations during the expansion of the fireball.

iii) The freeze-out concept is only a simplified approach and can be improved by more dynamical descriptions of the non-equilibrium time evolution during HIC.

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[1] J. P. Bondorf et al., Phys. Rept. 257, 133 (1995).
[2] A. Andronic, P. Braun-Munzinger, and J. Stachel, Nucl. Phys. A772, 167 (2006).
[3] S. Kowalski et al., Phys. Rev. C 75, 014601 (2007).
[4] Z. Kohley et al., Phys. Rev. C 83, 044601 (2011).
[5] L. Qin et al., Phys. Rev. Lett. 108, 172701 (2012).
[6] K. Hagel et al., Phys. Rev. Lett. 108, 062702 (2012).
[7] R. Wada et al., Phys. Rev. C 85, 064618 (2012).
[8] H. Zheng and A. Bonasera, Phys. Lett. B 696, 178 (2011); H. Zheng, G. Giuliani, and A. Bonasera, Nucl. Phys. A 892, 43 (2012); J. Mabiala et al., arXiv:1208.3480 [nucl-ex].
[9] S. Albergo et al., Nuovo Cimento A 89, 1 (1985).
[10] S. Shlomo et al., Phys. Rev. C 79, 034604 (2009).
[11] G. Röpke, Nucl. Phys. A 867, 66 (2011).
[12] A. Z. Mekjian, Phys. Rev. C 17, 1051 (1978); Phys. Rev. Lett. 38, 640 (1977).
[13] C. J. Horowitz and A. Schwenk, Nucl. Phys. A 776, 55 (2006).
[14] S. Typel et al., Phys. Rev. C 8, 015803 (2010).
[15] M. Hempel et al., Nucl. Phys. A 837, 210 (2010).
[16] J. B. Elliott et al., Phys. Rev. C 67, 024609 (2003); J. B. Elliott et al., arXiv:1203.5132 [subm. Phys. Rev. C].
[17] J.B. Natowitz et al., Int. J. Mod. Phys. E 13, 269 (2004).