Analysis of magnetic neutron-scattering data of two-phase ferromagnets

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We have analyzed magnetic-field-dependent small-angle neutron scattering (SANS) data of soft magnetic two-phase nanocomposite ferromagnets in terms of a recent micromagnetic theory for the magnetic SANS cross section [Honecker and Michels, Phys. Rev. B 87, 224426 (2013)]. The approach yields a value for the average exchange-stiffness constant and provides the Fourier coefficients of the magnetic anisotropy field and the magnetostatic field, which is related to jumps of the magnetization at internal interfaces.

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I. INTRODUCTION

Progress in the field of nanomagnetism1 relies on the continuous development and improvement of observational (microscopy and scattering) techniques. For instance, advances in spin-polarized scanning tunneling microscopy, electron microscopy and holography, Kerr microscopy, and synchrotron-based x-ray techniques such as x-ray magnetic circular dichroism allow one to resolve ever finer details of the magnetic microstructure of materials, with a spatial resolution that ranges from macroscopic dimensions down to the atomic scale (see, e.g., Ref. 2 and references therein).

The technique of neutron scattering is of particular importance for magnetism investigations, since it provides access to the structure and dynamics of magnetic materials on a wide range of length and time scales.3 Moreover, in contrast to electrons or light, neutrons are able to penetrate deeply into matter and, thus, enable the study of bulk properties.

Magnetic small-angle neutron scattering (SANS) measures the diffuse scattering along the forward direction which arises from nanoscale variations in the magnitude and orientation of the magnetization vector field \( \mathbf{M}(r) \). The measurable quantity in a magnetic SANS experiment—the (energy-integrated) macroscopic differential scattering cross section \( d\Sigma/d\Omega \)—depends on the Fourier coefficients of \( \mathbf{M}(r) \). These Fourier coefficients \( \mathbf{M}(q) \) depend in a complicated manner on the magnetic interactions, the underlying microstructure (e.g., particle-size distribution and crystallographic texture), and on the applied magnetic field. The continuum theory of micromagnetics8–10 provides the proper framework for computing \( d\Sigma/d\Omega \).11–13

In a recent paper14 we have derived closed-form expressions for the micromagnetic SANS cross section of two-phase particle-matrix-type bulk ferromagnets. Prototypical examples for this class of materials are hard and soft magnetic nanocomposite magnets, which consist of a dispersion of crystalline nanoparticles in a (crystalline or amorphous) magnetic matrix. Due to their technological relevance, e.g., as integral composite magnets, which consist of a dispersion of crystalline nanoparticles in a (crystalline or amorphous) magnetic matrix.

II. SANS THEORY

For the scattering geometry where the applied magnetic field \( \mathbf{H}_0 \parallel \mathbf{e}_z \) is perpendicular to the wave vector \( k_0 \) of the incoming neutron beam (see Fig. 1), the elastic (unpolarized) SANS cross section \( d\Sigma/d\Omega \) at scattering vector \( q \) can be written as6

\[
\frac{d\Sigma}{d\Omega}(q) = \frac{8\pi^3}{V} b_n^2 \left( \frac{|\tilde{\mathbf{M}}_y|^2}{b_n^2} + |\tilde{\mathbf{M}}_z|^2 \cos^2 \theta + |\tilde{\mathbf{M}}_y|^2 \sin^2 \theta - (\tilde{\mathbf{M}}_x \tilde{\mathbf{M}}_z + \tilde{\mathbf{M}}_y \tilde{\mathbf{M}}_z) \sin \theta \cos \theta \right),
\]  

where \( \tilde{\mathbf{M}}_i \) is the projection of the magnetization onto the scattering vector \( q \).
where $V$ is the scattering volume, $b_H = 2.9 \times 10^8 \text{A}^{-1} \text{m}^{-1}$, $\vec{N}(q)$ and $\vec{M}(q) = \{\vec{M}_u(q), \vec{M}_r(q), \vec{M}_l(q)\}$ denote, respectively, the Fourier coefficients of the nuclear scattering-length density and of the magnetization $\vec{M}(x) = \{M_u(x), M_r(x), M_l(x)\}$, and $\theta$ represents the angle between $\vec{H}_0$ and $\mathbf{q} \equiv \mathbf{q}(0, \sin \theta, \cos \theta)$; $c^*$ is a quantity complex-conjugated to $c$.

As shown in Ref. 14, near magnetic saturation and for a two-phase particle-matrix-type ferromagnet, $d \Sigma /d\Omega$ can be evaluated by means of micromagnetic theory. In particular,

$$
\frac{d \Sigma}{d\Omega}(\mathbf{q}) = \frac{d \Sigma_{\text{res}}}{d\Omega}(\mathbf{q}) + \frac{d \Sigma_{M}}{d\Omega}(\mathbf{q}),
$$

(2)

where

$$
\frac{d \Sigma_{\text{res}}}{d\Omega}(\mathbf{q}) = \frac{8 \pi^3}{V} b_H^2 \left( \frac{\vec{N}}{b_H^2} + |\vec{M}_l|^2 \sin^2 \theta \right)
$$

(3)

represents the (nuclear and magnetic) residual SANS cross section, which is measured at complete magnetic saturation (infinite field), and

$$
\frac{d \Sigma_{M}}{d\Omega}(\mathbf{q}) = S_H(\mathbf{q}) R_H(q, \theta, H_i) + S_M(\mathbf{q}) R_M(q, \theta, H_i)
$$

(4)

is the spin-misalignment SANS cross section. The magnetic scattering due to transversal spin components, with related Fourier amplitudes $\vec{M}_r(q)$ and $\vec{M}_l(q)$, is contained in $d \Sigma_{M}/d\Omega$, which decomposes into a contribution $S_H \times R_H$ due to perturbing magnetic anisotropies and a part $S_M \times R_M$ related to magnetostatic fields. The micromagnetic SANS theory considers a uniform exchange interaction and a random distribution of magnetic easy axes, but takes explicitly into account variations in the magnitude of the magnetization (via the function $S_M$, see below).

The anisotropy-field scattering function

$$
S_H(\mathbf{q}) = \frac{8 \pi^3}{V} b_H^2 |h|^2
$$

(5)

depends on the Fourier coefficient $h(\mathbf{q})$ of the magnetic anisotropy field, whereas the scattering function of the longitudinal magnetization

$$
S_M(\mathbf{q}) = \frac{8 \pi^3}{V} b_H^2 |\vec{M}_l|^2
$$

(6)

provides information on the magnitude $\Delta M \propto \vec{M}_l$ of the magnetization jump at internal (particle-matrix) interfaces. The corresponding (dimensionless) micromagnetic response functions can be expressed as

$$
R_H(q, \theta, H_i) = \frac{p^2}{2} \left( 1 + \frac{\cos^2 \theta}{(1 + p \sin^2 \theta)^2} \right),
$$

(7)

and

$$
R_M(q, \theta, H_i) = \frac{p^2}{2} \left( 1 + \frac{\cos^2 \theta}{(1 + p \sin^2 \theta)^2} \right) + \frac{2p^2}{4} \left( 1 + \frac{1}{\sqrt{1 + p}} \right),
$$

(8)

where $p(q, H_i) = M_s / H_{eff}$ and $\theta$ represents the angle between $\vec{H}_0$ and $\mathbf{q} \equiv \mathbf{q}(0, \sin \theta, \cos \theta)$. The effective magnetic field $H_{eff}(q, H_i) = H_i(1 + l_H^2 q^2)$ depends on the internal magnetic field $H_i$ and on the exchange length $l_H = (\sqrt{2}/\mu_0 M_s H_i) (M_s)$; saturation magnetization; $A$: exchange-stiffness parameter; $\mu_0 = 4 \pi \times 10^{-7} \text{Tm/A}$. The particular $\theta$ dependence of the transversal magnetization Fourier coefficients, Eqs. (15) and (16) in Ref. 14, and, hence, of $R_H$ and $R_M$ is essentially a consequence of the magnetodipolar interaction. Depending on the values of $q$ and $H_i$, a variety of angular anisotropies may be seen on a two-dimensional position-sensitive detector (compare also Fig. 11 in Ref. 13).

When the functions $\vec{N}$, $\vec{M}$, and $h$ depend only on the magnitude $q$ of the scattering vector, one can perform an azimuthal average of Eq. (2). The assumption that $\vec{M}_l$ is isotropic is supported by experiment26 and by micromagnetic simulations.12 The Fourier coefficient $h$ describes the spatial distribution (and magnitude) of magnetic anisotropy fields in the sample, and we believe that the assumption of isotropy is justified for the polycrystalline magnetic materials under study. The resulting expressions for the response functions then read

$$
R_H(q, H_i) = \frac{p^2}{4} \left( 1 + \frac{1}{\sqrt{1 + p}} \right),
$$

(9)

and

$$
R_M(q, H_i) = \sqrt{1 + p} - \frac{1}{2},
$$

(10)

so that the azimuthally-averaged total nuclear and magnetic SANS cross section can be written as

$$
\frac{d \Sigma}{d\Omega}(q) = \frac{d \Sigma_{\text{res}}}{d\Omega}(q) + S_H(q) R_H(q, H_i) + S_M(q) R_M(q, H_i),
$$

(11)
FIG. 3. (Color online) Qualitative comparison between experiment, analytical theory, and numerical micromagnetic simulations. Upper row: Experimental spin-misalignment SANS cross sections $d\Sigma_M/d\Omega$ of Fe$_{89}$Zr$_7$B$_3$Cu (Ref. 21) in the plane of the two-dimensional detector at selected applied magnetic fields (see insets). The $d\Sigma_M/d\Omega$ were obtained by subtracting the scattering at a saturating field of 1994 mT. $H_0$ is horizontal. Middle row: Prediction by the micromagnetic theory for $d\Sigma_M/d\Omega$, Eq. (4), at the same field values as above. For both $\tilde{M}_z(qR)$ and $h(qR)$ we have used the form factor of the sphere with a radius of $R = 6$ nm. Furthermore, the following materials parameters were used: $A = 3.1 \text{ J/m}$; $\mu_0M_s = 1.26$ T; $\mu_0H_p = 0.01$ T; $\mu_0\Delta M = 0.05$ T; this particular choice of parameters is motivated by the outcome of our data analysis (see below). Lower row: Results of full-scale three-dimensional micromagnetic simulations for $d\Sigma_M/d\Omega$ (Refs. 11–13). Linear color scale is used in all subfigures. For each data set, we have, respectively, normalized $d\Sigma_M/d\Omega$ to its highest value at the lowest field of 45 mT. Yellow color corresponds to “high” $d\Sigma_M/d\Omega$ and blue color to “low” values of $d\Sigma_M/d\Omega$.

For given values of the materials parameters $A$ and $M_s$, the numerical values of both response functions are known at each value of $q$ and $H_i$. Equation (11) is linear in both $R_H$ and $R_M$, with a priori unknown functions $d\Sigma_{res}/d\Omega$, $S_H$ and $S_M$. By plotting at a particular $q = q^*$ the values of $d\Sigma/d\Omega$ measured at several $H_i$ versus $R_H(q^*,H_i,A)$ and $R_M(q^*,H_i,A)$, one can obtain the values of $d\Sigma_{res}/d\Omega$, $S_H$ and $S_M$ at $q = q^*$ by (weighted) least-squares plane fits (see Fig. 2).}

Treating the exchange-stiffness constant in the expression for $H_{eff}$ as an adjustable parameter allows one to obtain information on this quantity. We note that in order to obtain a best-fit value for $A$ from experimental field-dependent SANS data, it is not necessary that the data is available in absolute units.
III. RESULTS AND DISCUSSION

Figure 3 provides a qualitative comparison between experiment, analytical theory, and numerical micromagnetic simulations for the field dependence of the spin-misalignment SANS cross section $d\Sigma_M/d\Omega$. The purpose of this figure is to demonstrate that the experimental anisotropy ($\theta$ dependence) of $d\Sigma_M/d\Omega$ (upper row in Fig. 3) can be well reproduced by the theory. At the largest fields, one observes the so-called clover-leaf anisotropy with maxima in $d\Sigma_M/d\Omega$ roughly along the diagonals of the detector. Clearly, this feature is due to the term $S_M \times R_M$ in $d\Sigma_M/d\Omega$ [compare Eq. (8)]. Reducing the field results in the emergence of a scattering pattern that is more of a $\cos^2 \theta$-type (with maxima along the horizontal direction). The observed transition in the experimental data is qualitatively reproduced by the analytical micromagnetic theory (middle row, compare also Figs. 2 and 3 in Ref. 14), and by the results of full-scale three-dimensional micromagnetic simulations for $d\Sigma_M/d\Omega$ (lower row). For further details on the micromagnetic simulation methodology, we refer the reader to Refs. 11–13.

The observation that the anisotropy in the experimental 163 mT data is not as clearly visible as in the other two data sets is related to the fact that (i) both analytical theory and micromagnetic simulations do not contain instrumental smearing effects (in contrast to the experimental data), and that (ii) the displayed difference-intensity data was obtained by subtracting the scattering at the highest field ($\sim 2$ T), which may not be sufficient to completely saturate the sample. By contrast, in the theory and the simulations the scattering at saturation can be obtained precisely and the subtraction procedure yields the pure spin-misalignment scattering cross section. Furthermore, we note that for the sake of a rough qualitative comparison (visualization), we have used in the analytical theory the simple sphere form factor for both $M_s(qR)$ and $h(qR)$. Spin canting, which is known to be of relevance in nanoparticles,\textsuperscript{28} may be modeled, e.g., via a core-shell form factor. Likewise, in view of the large particle volume fraction of both samples, a structure factor may also be included, but we believe that this will not contribute significantly to obtaining a more detailed understanding of the field and $\theta$ dependence of $d\Sigma_M/d\Omega$, since this rather affects the $\theta$ dependence of $d\Sigma_M/d\Omega$, which is analyzed in the following.

The azimuthally-averaged field-dependent SANS cross sections of both Nanoperm samples along with the fits to the micromagnetic theory [Eq. (11), solid lines] are displayed in Figs. 4(a) and 4(b). It is seen that for both samples the entire $(q, H)$ dependence of $d\Sigma_M/d\Omega$ can be excellently described by the micromagnetic prediction. As expected, both residual SANS cross sections $d\Sigma_{res}/d\Omega$ ($\circ$) are smaller than the respective total $d\Sigma_M/d\Omega$, supporting the notion of dominant spin-misalignment scattering in these types of materials. From the fit of the entire $(q, H)$ data set to Eq. (11) one obtains values for the volume-averaged exchange-stiffness constants [compare insets in Figs. 4(a) and 4(b)]. We obtain $A = 3.1 \pm 0.1$ pJ/m for the Co-free alloy and $A = 4.7 \pm 0.9$ pJ/m for the zero-magnetostrection Nanoperm sample.

Since jumps in $A$ have not been taken into account in our micromagnetic SANS theory, the determined $A$ values represent mean values, averaged over crystalline and amorphous regions within the sample. The thickness $\delta$ of the intergranular amorphous layer between the iron nanoparticles can be roughly estimated by\textsuperscript{29} $\delta = D(x_C^{-1/3} - 1)$, where $D$ is the average particle size and $x_C$ denotes the crystalline volume fraction. For Fe$_{89}$Zr$_7$B$_3$Cu with $D = 12$ nm and $x_C = 40\%$ we obtain $\delta \cong 4$ nm, whereas $\delta \cong 2$ nm for (Fe$_{98.5}$Co$_{0.5}$)$_{10}$Zr$_7$B$_3$ with $D = 15$ nm and $x_C = 65\%$. Since one may expect that the effective exchange stiffness is governed by the weakest link in the bcc-amorphous-bcc coupling chain,\textsuperscript{15,30} the above determined experimental values for $A$ reflect qualitatively the trend in $\delta$ (and hence in $x_C$) between the two samples.
The experimental $A$ values seem to be in agreement with the following expression for the effective exchange-stiffness constant $A$ of two-phase magnetic nanostructures,$^{35}$

$$\frac{D + \delta}{\sqrt{A}} = \frac{D}{\sqrt{A_{cr}}} + \frac{\delta}{\sqrt{A_{am}}}, \quad (12)$$

where $A_{cr}$ and $A_{am}$ denote, respectively, the local exchange constants of the crystalline iron and amorphous matrix phase. Equation (12) has been derived by considering the behavior of the tilting angle between exchange-coupled local magnetizations.$^{30}$ $A_{am}$ can be roughly estimated by means of $A_{am} = A_{cr} \left( \frac{M^2_{am}}{M^2_{cr}} \right)^\frac{2}{3} \frac{T^m_{cr}}{T^m_{am}}$, where $A_{cr} = 10 \text{ pJ/m}$, $\mu_0 M^2_{cr} = 2.15 \text{ T}$, $T^c_{cr} = 1043 \text{ K (Ref. 31)}$, and $T^m_{am} \cong 350 \text{ K (Ref. 30)}$; $M^2_{am}$ is found by using the measured $M^2_{cr}$-value of the compound and the crystalline volume fraction, according to $M^2_{cr} = (M^2 - M^2_{am})(1 - \chi_C)$. By inserting these estimates in Eq. (12), we finally obtain effective values of $A = 2.1 \text{ pJ/m}$ ($\text{Fe}_{89}\text{Zr}_{7}\text{B}_{3}\text{Cu}$) and $A = 4.0 \text{ pJ/m}$ ($\text{Fe}_{0.985}\text{Co}_{0.015}\text{Zr}_7\text{B}_3$), which agree reasonably with the experimental data.

In addition to the exchange-stiffness constant, analysis of field-dependent SANS data in terms of Eq. (11) provides the magnitude squares of the Fourier coefficients of the magnetic anisotropy field $S_H \propto |h(q)|^2$ and of the longitudinal magnetization $S_M \propto |\bar{M}(q)|^2 \propto (\Delta M)^2$ (see Fig. 5). It is immediately seen in Fig. 5 that over most of the displayed $q$-range $|\bar{M}|^2$ is orders of magnitude larger than $|h|^2$, suggesting that jumps $\Delta M$ in the magnetization at internal interfaces is the dominating source of spin disorder in these alloys. For $\text{Fe}_{89}\text{Zr}_{7}\text{B}_{3}\text{Cu}$ at the largest $q$, the Fourier coefficient $|h|^2$ becomes comparable to $|\bar{M}|^2$ [Fig. 5(a)]. This explains the existence of the $\cos^2 \theta$-type anisotropy in $dS_M/d\Omega$ at the smallest fields (compare Fig. 3).

Numerical integration of $S_H(q)$ and $S_M(q)$ over the whole $q$ space, i.e.,

$$\frac{1}{2\pi^2 b^2 H} \int_0^{\infty} S_{H,M} q^2 dq,$$

yields, respectively, the mean-square anisotropy field $\langle |H|^2 \rangle$ and the mean-square longitudinal magnetization fluctuation $\langle M^2 \rangle$ (e.g., Ref. 32). However, since experimental data for $S_H$ and $S_M$ are only available within a finite range of momentum transfers (between $q_{min}$ and $q_{max}$) and since both integrands $S_H q^2$ and $S_M q^2$ do not show signs of convergence, one can only obtain rough lower bounds for these quantities:

For the ($\text{Fe}_{0.985}\text{Co}_{0.015}\text{Zr}_7\text{B}_3$) sample (for which $d\Sigma/d\Omega$ is available in absolute units), we obtain $\mu_0 \langle |H|^2 \rangle^{1/2} \cong 10 \text{ mT}$ and $\mu_0 \langle M^2 \rangle^{1/2} \cong 50 \text{ mT}$. This finding qualitatively supports the notion of dominant spin-misalignment scattering due to magnetostatic fluctuations. Finally, we note that knowledge of $S_H \propto |\bar{M}|^2$ and of the residual SANS cross section $d\Sigma_{res}/d\Omega$ [Eq. (3)] allows one to obtain the nuclear scattering $|N|^2$ (see Fig. 5), without using sector-averaging procedures (in unpolarized scattering) or polarization analysis.$^{26}$

IV. SUMMARY AND CONCLUSIONS

We have analyzed magnetic-field-dependent SANS data of iron-based soft magnetic nanocomposites in terms of a recent micromagnetic theory for the magnetic SANS cross section. The approach provides quantitative results for the mean exchange-stiffness constant as well as for the Fourier coefficients of the magnetic anisotropy field and the longitudinal magnetization. The observed angular anisotropy of the SANS pattern, in particular, the clover-leaf anisotropy, can be well reproduced by the theory. For the two Nanoperm alloys under study, we find evidence that the magnetic microstructure close to saturation is dominated by jumps in the magnetization at internal interfaces. A lower bound for the root-mean-square longitudinal magnetization fluctuation of $\sim 50 \text{ mT}$ could be estimated, as compared to a mean magnetic anisotropy field of strength $\sim 10 \text{ mT}$. 

FIG. 5. (Color online) Best-fit results for the scattering function of the anisotropy field $S_H = 8\pi^3 V^{-1} b^2 H |h(q)|^2$ and for the scattering function of the longitudinal magnetization $S_M = 8\pi^3 V^{-1} b^2 H |\bar{M}(q)|^2$ of (a) $\text{Fe}_{89}\text{Zr}_{7}\text{B}_{3}\text{Cu}$ and (b) ($\text{Fe}_{0.985}\text{Co}_{0.015}\text{Zr}_7\text{B}_3$) (log-log scale). $d\Sigma_{res}/d\Omega = 8\pi^3 V^{-1} |N|^2$ denotes the nuclear SANS, which was, respectively, obtained by subtracting the $|\bar{M}|^2$ scattering from the residual SANS cross section $d\Sigma_{res}/d\Omega$ [compare Eq. (3)].
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