Abstract: In this paper, the adapted \((G'/G)\)-expansion scheme is executed to obtain exact solutions to the fractional Clannish Random Walker’s Parabolic (FCRWP) equation. Some innovative results of the FCRWP equation are gained via the scheme. A diverse variety of exact outcomes are obtained. The proposed procedure could also be used to acquire exact solutions for other nonlinear fractional mathematical models (NLFMMs).

Keywords: FCRWP; adapted \((G'/G)\)-expansion scheme; exact solutions; fractional calculus; nonlinear dynamics

1. Introduction

Nonlinear fractional mathematical models (NLFMMs) are widely employed to describe many substantial phenomena and fractional nonlinear dynamic applications in plasma physics, mathematics, nonlinear control theory, physics, stochastic dynamical systems, engineering, signal processing, image processing, electromagnetics, transport systems, communications, acoustics, genetic algorithms, and viscoelasticity, amongst others. To define the exact answers to NLFMMs, many dominant and well-organized systems have been constructed and popularized, such as the variation of the \((G'/G)\)-expansion scheme [1], adapted \((G'/G)\)-expansion technique [2–5], exponential ansatz method [6], fractional iteration algorithm [7,8], the unified method [9], the first integral technique [10], the subequation scheme [11], improved fractional subequation scheme [12], the Jacobi elliptic ansatz method [13], generalized Kudryashov technique [14,15], novel extended direct algebraic method [16], natural transform method [17], fractional sub-equation scheme [18], exp-task scheme [19], generalized exponential rational task scheme [20], Kudryashov technique [21], sine-Gordon expansion technique [22], and the Jacobi elliptic task scheme [23]. Ma et al. [24] recently discovered a profoundly significant enlargement of the \((G'/G)\)-extension process, called the adapted \((G'/G)\)-extension process, to secure exact solutions to NLFMMs. We used the adapted \((G'/G)\)-extension process for providing exact answers to the fractional Clannish Random Walker’s Parabolic (FCRWP) equation in an ongoing effort to express it using a suitable and simple process. Therefore, we effortlessly exchange the FCRWP equation into a nonlinear partial differential equation (NPDE) or nonlinear ordinary differential equation (NODE) via the appropriate conversion to facilitate the
process for those acquainted with fractional calculus. The main advantage of the process implemented in this study compared with the basic \((G'/G)\)-extension scheme is that it contributes additional novel exact answers, including added independent parameters. The implemented process takes all the responses received by the basic \((G'/G)\)-extension scheme as a particular event, and we generate a few novel results. The exact answers are significant for uncovering the fundamental devices of physical events. Apart from the dynamic relevance, the exact answers to NLFMMs support numerical solvers when comparing their results’ accuracies and help them in the stability analysis.

The remainder of this paper is organized as follows: In Section 2, we present a few analyses of the adapted \((G'/G)\)-expansion scheme. In Section 3, we obtain answers to the FCRWP equation via the suggested method. In Section 4, we present some numerical simulations of the obtained solutions. In the last section, we present our conclusions.

2. Glimpse of the Technique

First, we provide a few ideas from fractional calculus theory and then present our proposed technique. For an outline of fractional calculus, we refer the reader to Refs. \([25–27]\). Numerous distinct varieties of fractional derivative operators have been recognized, such as: Atangana–Baleanu derivative \([28]\), the Mittag–Leffler matrix function \([29]\), Caputo–Fabrizio \([30]\), the fractional boundary value problem with Sturm–Liouville boundary conditions \([31]\), the Caputo derivative \([27]\), the fractional derivative \([32]\), and the conformable derivative \([33]\). Now, we concisely analyze the modified Riemann–Liouville derivative (MRLD) from the current fractional calculus recommended by Jumarie \([34,35]\). This leads to our study technique. Let \(S : [0, 1] \rightarrow \mathbb{R} \) be a continuous function and \(\beta \in (0, 1)\). The Jumarie-improved fractional derivative of order \(\beta \) and \(S \) might be well-defined by \([36]\)

\[
D_x^\beta S(x) = \begin{cases} 
\frac{1}{\Gamma(\beta-1)} \int_0^x (x-\chi)^{\beta-1} [S(\chi) - S(0)] d\chi, & \text{if } \beta > 1, \\
\frac{1}{\Gamma(\beta-1)} \frac{d}{dx} \int_0^x (x-\chi)^{\beta-1} [S(\chi) - S(0)] d\chi, & \text{if } 0 < \beta < 1, \\
(S^{(n)}(x))/(\beta-n), & n \leq \beta \leq n+1, \ n \geq 1.
\end{cases}
\]

In addition to this representation, we preliminarily describe some properties of the fractional MRLD, which are later implemented in this paper. A few of the convenient procedures are assumed as:

\[
D_x^\beta 0 = 0 \quad (A \text{ is a constant})
\]

\[
D_x^\beta x^B = \begin{cases} 
0, & \text{if } B \leq \beta - 1, \\
\Gamma(B+1) x^{\beta-B}, & \text{if } B > \beta - 1.
\end{cases}
\]

\[
D_x^\beta (C_1 R(x) + C_2 S(x)) = C_1 D_x^\beta R(x) + C_2 D_x^\beta S(x), \quad (C_1 \text{ and } C_2 \text{ are constants})
\]

\[
D_x^\beta (S(x) R(x)) = S(x) D_x^\beta R(x) + R(x) D_x^\beta S(x),
\]

\[
S(x) = \sum_{A=0}^{\infty} \left( \frac{n}{A} \right) R^{(A)}(x) D_x^{\beta-A} S(x),
\]

\[
D_x^\beta [T(S(x))] = T_x^\beta (S(x)) = D_x^\beta T(S(x)) = D_x^\beta T(S(x))^{\beta}, dt^\beta x(t) = \Gamma(1 + \beta) d\chi(t).
\]

We consider

\[
P(\Lambda, \Lambda_x, \Lambda_{xx}, \Lambda_t, \Lambda_{tt}, \ldots) = 0,
\]

where \(P\) is a polynomial in \(\Lambda\) and its partial derivatives.

Firstly, use the travelling variable:

\[
\Lambda = \Lambda(x,t) = \Lambda(\chi), \chi = p_3(x - Vt),
\]
where \( p_3 \) and \( V \) are constants to be determined later. Substituting Equation (8) into Equation (7), we obtain:

\[
R(\lambda, p_3\lambda', p_3^2\lambda'', -p_3V\lambda', p_3^2V^2\lambda'', -p_3^2V^2\lambda'', \ldots) = 0. \tag{9}
\]

Firstly, considering the ansatz form:

\[
\lambda(\chi) = \sum_{i=-M}^{M} S_i h_i \tag{10}
\]

where \( h = \left( \frac{G'}{G} + \frac{\lambda}{2} \right), |S_{-M}| + |S_M| \neq 0, \) and \( G = G(\chi) \) satisfy the equation.

\[
G'' + \lambda G' + \mu G = 0, \tag{11}
\]

where \( S_i(\pm 1, \pm 2, \ldots, \pm M) \), and \( \lambda \) and \( \mu \) are coefficient constants defined later. Implementing the homogeneous balance principle in Equation (9), the positive integer \( M \) can be determined. From Equation (11), we find that \( \bar{h}' = r - \bar{h}^2 \), \( \bar{r} = \lambda^2 - 4\mu \), and \( r \) is calculated by \( \lambda \) and \( \mu \). So, \( \bar{h} \) satisfies Equation (12), which produces:

\[
\begin{align*}
&h = \begin{cases} 
\sqrt{r} \tanh(\sqrt{r} \chi), & r > 0; \\
\sqrt{r} \coth(\sqrt{r} \chi), & r > 0; \\
\frac{1}{2}, & r = 0; \\
-\sqrt{r} \tan(\sqrt{-r} \chi), & r < 0; \\
-\sqrt{r} \cot(\sqrt{-r} \chi), & r < 0.
\end{cases}
\end{align*} \tag{13}
\]

Finally, by implementing Equations (9) and (10) and collecting all terms with the same order of \( \bar{h} \) together, the left-hand side of Equation (10) is converted into a polynomial in \( \bar{h} \). Equating each coefficient of the polynomial to zero, we can obtain a set of algebraic equations that can be solved to find the values of the studied method.

3. Mathematical Analysis

In this paper, we consider the FCRWP equation [37]:

\[
\frac{\partial^\beta A}{\partial t^\beta} - \frac{\partial A}{\partial x} + 2\lambda\frac{\partial A}{\partial x} + \frac{\partial^2 A}{\partial x^2} = 0, \ t > 0, 0 < \beta, \tag{14}
\]

with \( A(x, 0) = S(x) \). Taking the variable transformation \( A(x, t) = A(\chi), \chi = x - \frac{Vt}{1+\beta} \), in Equation (14), we have:

\[
-V\lambda' - \lambda + 2\lambda\lambda' - \lambda'' = 0. \tag{15}
\]

The pole of Equation (15) is given as \( N = 1 \). Then, we find from Equation (10) that:

\[
A(\chi) = \sum_{i=-1}^{1} S_i h_i \tag{16}
\]

Collecting the coefficient of Equation (14) and finding the resulting system, we then find:

Group I : \( V = 2S_0 - 1, S_1 = 0, S_{-1} = -\frac{1}{4}\lambda^2 + \mu. \) \tag{17}

Substituting the above values into Equation (15), we obtain:

\[
A_{11}(\chi) = S_0 + \left( -\frac{1}{4}\lambda^2 + \mu \right) \times \left\{ \frac{\sqrt{\lambda^2 - 4\mu}}{2} \tanh\left( \frac{\sqrt{\lambda^2 - 4\mu}}{2} \chi \right) \right\}^{-1}. \tag{18}
\]
\[ 
\begin{align*}
\mathcal{A}_{12}(\chi) &= S_0 + \left(-\frac{1}{4}\lambda^2 + \mu\right) \times \left\{ \frac{\sqrt{\lambda^2 - 4\mu}}{2} \coth \left( \frac{\sqrt{\lambda^2 - 4\mu}}{2} \right) \right\}^{-1}. \\
\mathcal{A}_{13}(\chi) &= S_0 + \left(-\frac{1}{4}\lambda^2 + \mu\right) \times \left(\frac{1}{\lambda}\right)^{-1}. \\
\mathcal{A}_{14}(\chi) &= S_0 + \left(-\frac{1}{4}\lambda^2 + \mu\right) \times \left\{ -\frac{\sqrt{4\mu - \lambda^2}}{2} \tan \left( \frac{\sqrt{4\mu - \lambda^2}}{2} \right) \right\}^{-1}. \\
\mathcal{A}_{15}(\chi) &= S_0 + \left(-\frac{1}{4}\lambda^2 + \mu\right) \times \left\{ -\frac{\sqrt{4\mu - \lambda^2}}{2} \cot \left( \frac{\sqrt{4\mu - \lambda^2}}{2} \right) \right\}^{-1}, \\
\end{align*} 
\]

Similarly, we obtain:

\[ 
\begin{align*}
\mathcal{A}_{21}(\chi) &= S_0 - \left\{ \frac{\sqrt{\lambda^2 - 4\mu}}{2} \tanh \left( \frac{\sqrt{\lambda^2 - 4\mu}}{2} \right) \right\} \\
\mathcal{A}_{22}(\chi) &= S_0 - \left\{ \frac{\sqrt{\lambda^2 - 4\mu}}{2} \coth \left( \frac{\sqrt{\lambda^2 - 4\mu}}{2} \right) \right\}. \\
\mathcal{A}_{23}(\chi) &= S_0 - \left(\frac{1}{\lambda}\right). \\
\mathcal{A}_{24}(\chi) &= S_0 - \left\{ -\frac{\sqrt{4\mu - \lambda^2}}{2} \tan \left( \frac{\sqrt{4\mu - \lambda^2}}{2} \right) \right\}. \\
\mathcal{A}_{25}(\chi) &= S_0 - \left\{ -\frac{\sqrt{4\mu - \lambda^2}}{2} \cot \left( \frac{\sqrt{4\mu - \lambda^2}}{2} \right) \right\}. \\
\end{align*} 
\]

Group II: \( V = 2S_0 - 1, S_1 = -1, S_{-1} = -\frac{1}{4}\lambda^2 + \mu. \)

Similarly, we obtain:

\[ 
\begin{align*}
\mathcal{A}_{31}(\chi) &= S_0 - \left\{ \frac{\sqrt{\lambda^2 - 4\mu}}{2} \tanh \left( \frac{\sqrt{\lambda^2 - 4\mu}}{2} \right) \right\} \\
&\quad + \left(-\frac{1}{4}\lambda^2 + \mu\right) \times \left\{ \frac{\sqrt{\lambda^2 - 4\mu}}{2} \coth \left( \frac{\sqrt{\lambda^2 - 4\mu}}{2} \right) \right\}^{-1}. \\
\mathcal{A}_{32}(\chi) &= S_0 - \left\{ \frac{\sqrt{\lambda^2 - 4\mu}}{2} \coth \left( \frac{\sqrt{\lambda^2 - 4\mu}}{2} \right) \right\} \\
&\quad + \left(-\frac{1}{4}\lambda^2 + \mu\right) \times \left\{ \frac{\sqrt{\lambda^2 - 4\mu}}{2} \coth \left( \frac{\sqrt{\lambda^2 - 4\mu}}{2} \right) \right\}^{-1}. \\
\mathcal{A}_{33}(\chi) &= S_0 - \left(\frac{1}{\lambda}\right) + \left(-\frac{1}{4}\lambda^2 + \mu\right) \times \left(\frac{1}{\lambda}\right)^{-1}. \\
\mathcal{A}_{34}(\chi) &= S_0 - \left\{ -\frac{\sqrt{4\mu - \lambda^2}}{2} \tan \left( \frac{\sqrt{4\mu - \lambda^2}}{2} \right) \right\} \\
&\quad + \left(-\frac{1}{4}\lambda^2 + \mu\right) \times \left\{ -\frac{\sqrt{4\mu - \lambda^2}}{2} \tan \left( \frac{\sqrt{4\mu - \lambda^2}}{2} \right) \right\}^{-1}. \\
\mathcal{A}_{35}(\chi) &= S_0 - \left\{ -\frac{\sqrt{4\mu - \lambda^2}}{2} \cot \left( \frac{\sqrt{4\mu - \lambda^2}}{2} \right) \right\} \\
&\quad + \left(-\frac{1}{4}\lambda^2 + \mu\right) \times \left\{ -\frac{\sqrt{4\mu - \lambda^2}}{2} \cot \left( \frac{\sqrt{4\mu - \lambda^2}}{2} \right) \right\}^{-1}. \\
\end{align*} 
\]

4. Numerical Simulations

Ma et al. [24] introduced a process named the revised \((G'/G)\)-extension approach to look for the FCRWP equation’s exact structures and achieved fifteen results, shown in Section 3. Gunner et al. [37] reported a process named the \((G'/G)\)-extension approach to look for the FCRWP equation’s exact structures and achieved three results. In comparing the two methods, the revised \((G'/G)\)-extension approach provides a more exact answer than the \((G'/G)\)-extension approach. In terms of additional support, the auxiliary model
employed in the integral method is different, so the exact structures obtained are also different. Likewise, for any NLFMM, it could be determined that the revised \((G'/G)\)-extension approach is much more straightforward than the other schemes. In this paper, the integrable method is applied to the FCRWP equation for the first time. We confirm that no other author has used the technique on the FCRWP equation. This paper expresses various varieties of exact solutions of the answers for countless values of the constant coefficients. The exact solutions are: dark soliton profiles, singular kink profiles, dark singular soliton profiles, bright and dark lump shapes, periodic wave profiles, etc. Furthermore, we offer a contour graph of the obtained answers, which was created by commencing binary variable tasks. One variable is demonstrated on the horizontal and vertical axes of the contour graph. The functional value exemplifies the color gradient and isolines. The contour graph is a technique used to express a 3D surface on a 2D plane. This kind of graph is broadly implemented in mathematics, physics, as well as engineering, where the contour lines normally represent elevation. We obtained exact solutions like trigonometric, hyperbolic, and rational function solutions through the proposed procedure. The solutions \(\lambda_{11}(\chi), \lambda_{12}(\chi), \lambda_{21}(\chi), \lambda_{22}(\chi), \lambda_{31}(\chi), \lambda_{32}(\chi)\) present as trigonometric function solutions; the solutions of \(\lambda_{14}(\chi), \lambda_{15}(\chi), \lambda_{24}(\chi), \lambda_{25}(\chi), \lambda_{34}(\chi), \lambda_{35}(\chi)\) present as hyperbolic function solutions; and the solutions of \(\lambda_{13}(\chi), \lambda_{23}(\chi), \lambda_{33}(\chi)\) present as trigonometric function solutions. We explain the dynamic performance of the trigonometric function answers of \(\lambda_{11}(\chi), \lambda_{12}(\chi), \lambda_{22}(\chi), \lambda_{31}(\chi)\), which are illustrated in Figures 1–4. In particular, Figures 1–4 demonstrate the 3D shape, contour plot, and 2D graph for different values of \(\alpha\) for the trigonometric function answers of \(\lambda_{11}(\chi), \lambda_{12}(\chi), \lambda_{22}(\chi), \lambda_{31}(\chi)\). We explain the dynamic performance of the rational function answers to \(\lambda_{23}(\chi)\) and \(\lambda_{33}(\chi)\), as illustrated in Figures 5 and 6. Figures 5 and 6 demonstrate the 3D shape, contour plot, and 2D graph for different values of \(\alpha\) for the rational function answers to \(\lambda_{23}(\chi)\) and \(\lambda_{33}(\chi)\). Finally, we explain the dynamic performance of the trigonometric function answers of \(\lambda_{14}(\chi), \lambda_{15}(\chi), \lambda_{25}(\chi), \lambda_{34}(\chi)\) in Figures 7–10, which depict the 3D shape, contour plot, and 2D graph for different values of \(\alpha\) for the trigonometric function answers of \(\lambda_{14}(\chi), \lambda_{15}(\chi), \lambda_{25}(\chi), \lambda_{34}(\chi)\). The implemented mathematical simulations acknowledge that the answers are of periodic wave shapes and of rational, hyperbolic, and trigonometric categorizations. Furthermore, through observing the construction of the acquired answers, it could be understood that the connecting fractional derivatives of parameter \(\alpha\) perform in the formulation of all the answers.

Figure 1. The graphical representation of the solution \(\lambda_{11}(\chi)\): (a) 3D shape, (b) contour plot, and (c) 2D graph.
Figure 2. The graphical representation of the solution $A_{12}(\chi)$: (a) 3D shape, (b) contour plot, and (c) 2D graph.

Figure 3. The graphical representation of the solution $A_{22}(\chi)$: (a) 3D shape, (b) contour plot, and (c) 2D graph.

Figure 4. The graphical representation of the solution $A_{31}(\chi)$: (a) 3D shape, (b) contour plot, and (c) 2D graph.
Figure 5. The graphical representation of the solution $\lambda_{23}(\chi)$: (a) 3D shape, (b) contour plot, and (c) 2D graph.

Figure 6. The graphical representation of the solution $\lambda_{33}(\chi)$: (a) 3D shape, (b) contour plot, and (c) 2D graph.

Figure 7. The graphical representation of the solution $\lambda_{14}(\chi)$: (a) 3D shape, (b) contour plot, and (c) 2D graph.
Figure 8. The graphical representation of the solution $\lambda_{15}(\chi)$: (a) 3D shape, (b) contour plot, and (c) 2D graph.

Figure 9. The graphical representation of the solution $\lambda_{25}(\chi)$: (a) 3D shape, (b) contour plot, and (c) 2D graph.

Figure 10. The graphical representation of the solution $\lambda_{34}(\chi)$: (a) 3D shape, (b) contour plot, and (c) 2D graph.

5. Conclusions

In this investigation, we successfully devised a procedure that demonstrates that this system is well-organized and effectively acceptable for finding the exact answers to the FCRWP equation. A wide variety of dynamical behaviors were considered in this study, which presented in well-defined regions of mathematical physics. The most important advantage of this method is that it can more easily reach the solutions than the other analytical schemes for solving NLFMMs. These answers will be valuable for further studies in mathematical physics.
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