Designing coupled microcavity lasers for high-Q modes with unidirectional light emission

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We design coupled optical microcavities and report directional light emission from high-Q modes for a broad range of refractive indices. The system consists of a circular cavity that provides a high-Q mode in form of a whispering gallery mode, whereas an adjacent deformed microcavity plays the role of a waveguide or collimator of the light transmitted from the circular cavity. As a result of this very simple, yet robust, concept we obtain high-Q modes with promising directional emission characteristics. No information about phase space is required, and the proposed scheme can be easily realized in experiments.

Figure 1(a) shows our system which consists of two cavities with different boundary shapes: a circular cavity (left, radius $R_L$) and a circular-elliptic cavity (right, see text for details). (b) Unidirectional light emissions of light emanating from the focus point of an elliptic cavity with eccentricity being the inverse of its refractive index.

In this Letter we report a scheme that overcomes the drawbacks of two-disk microcavities and the limited range of working refractive indices for Limaçon-shaped devices, yet keeping their robustness. Our design couples a circular cavity with a deformed disk, cf. Fig. 1.

Figure 1. (Color online) (a) Coupled-disk microcavity laser consisting of a circular cavity (left, radius $R_L$) and a circular-elliptic cavity (right, see text for details).
The critical value determining unidirectional emission is the ratio between the intensity emitted into a 90 degree polarization in the range $20^\circ$ and the total emitted intensity. In order to check whether the result developed above.

As shown in Ref. [24], optical tunneling into the other (right) disk determines the low-intensity tail structure of these WGMs. It is characterized by two properties. First, optical tunneling occurs predominately near the closest approach of the two cavities. Second, the transmitted light has the same angular momentum profile as the WGM in the left disk, provided the two disks are sufficiently close. These two properties provide all the information needed to describe the position and angular momentum profile of the initial light on the right disk, and we can obtain the resulting far-field pattern using ray optics as described below. Note that the characteristics of the initial light in the second cavity derived in Refs. [24][26] for non-identical microdisk laser, is valid in our generalized system because the boundary shape in the area of optical tunneling is circular on either side.

The ray dynamics of the light initiated in the right cavity is then as follows. The light originates from the focus of the ellipse, which is part of the circular arc in Fig. 1(a) and reaches the cavity boundary in its elliptic part (other light rays are neglected) where the light makes the first dominant transmission through the dielectric interface. Geometric optics for a dielectric ellipse with $\epsilon = 1/n$ yields [29] that all these rays are emitted into the same direction, namely into a far-field angle of $\phi = 0$. This situation is depicted in Fig. 1(b) for a fully elliptic cavity with light emerging from the left focal point.

This geometric optics consideration suggests an intricate interplay between the light in both cavities also in a wave description. In order to check whether the resulting mode, expected to emit directional into the $\phi = 0$ direction, still has the high $Q$-factor of the initial WGM, we investigate the relation between $Q$-factor and unidirectionality. To this end we define the unidirectionality factor $U$ as

$$U = \frac{\int_{-\pi}^{\pi} I(\phi) d\phi}{\int_{-\pi}^{\pi} I(\phi) d\phi} = \frac{\int_{-\pi}^{\pi} I(\phi) d\phi}{\int_{-\pi}^{\pi} I(\phi) d\phi},$$

where $I(\phi)$ is the light intensity at the far-field angle $\phi$ and we set $\Phi = \pi/4$ in the following, i.e., we consider the ratio between the intensity emitted into a 90 degree window around $\phi = 0$ and the total emitted intensity. The critical value determining unidirectional emission is therefore an $U$-factor larger than 0.25. Modes with $U$ sufficiently larger than 0.25, and ideally $U$ close to the maximum value 1, possess thus the best unidirectional emission properties.

Figure 2(a) shows the relation between $U$- and $Q$-factor for resonant modes of transverse magnetic (TM) polarization in the range $20 < \text{Re}(nkR_L) < 30$ ($k$ is the wave number in vacuum) for $n = 3.3$ and $d = 0.1$, which is obtained numerically using the boundary element method [30]. Notably, $U$ increases (on average) with $Q$, and we find that a high unidirectional factor $U$ can indeed be combined with a high $Q$-factor, as desired: Most of the high-$Q$ modes have $U$-factors $U > 0.25$, whereas the $U$-factor of the low-$Q$ modes is distributed around the critical value with a considerable variance. This result proves the relevance of the ray-optics argument developed above.

Examples for high-$Q$, unidirectional emitting modes are indicated by the red triangle and square in Fig. 2(a). Their near- and far-field patterns, shown in Figs. 2(b),(d) and (c),(e), respectively, confirm the existence of a WGM localized on the left disk and the unidirectional light emission from the right, deformed cavity. Although the low-intensity tail structures in the right cavities differ for the two modes – it is a localized pattern in Fig. 2(b) and a more complex pattern in Fig. 2(d) –, the directionalities of both far-field patterns are very similar as shown in Figs. 2(c) and (e).

Very similar behavior is found for coupled cavities with refractive index $n = 2$, see Fig. 2(f) to (j). Note that robust unidirectional emission in the proposed scheme is achieved by adjusting the boundary geometry according to the refractive index $n$ [cf. the insets in Fig. 2(a)] and (f) and holds, moreover, even for slight deviations in shape and/or $n$. No information about phase space is needed in contrast to single-cavity lasers where the unstable manifold [20][23] typically provides the basis to
design unidirectional emission properties. Consequently, their emission properties strongly depend on the refractive index $n$ - namely on the way the critical line for total internal reflection intersects with the unstable manifold, and for a given geometry, unidirectionality is limited to a certain range of refractive indices. The design introduced here works, however, for a broad range of refractive indices ($n \gtrsim 2.0$) and is therefore applicable to a variety of materials, another useful property adding to the overall robustness of the proposed method.

In principle, we can adjust the $U$- and $Q$-factor of a mode by controlling the interdisk distance $d$. This is shown in Fig. 3 for the six highest-$Q$ modes as a function of $d$ for $n = 3.3$. For small $d$, especially for $d$ in the vicinity of half the vacuum wavelength, we find good directionality ($U > 0.5$), but the $Q$-factor starts to spoil. As $d$ increases and exceeds the mode wavelength, the $U$-factor approaches the critical value 0.25 for isotropic emission, and the $Q$-factor the one of single microdisk WGMs, confirming that optical tunneling as the backbone of the proposed design is lost. We point out that $U$ tends to decrease slightly for very small $d$ ($d$ significantly smaller than half the mode wavelength) due to modifications in tunneling.

We have designed coupled optical microcavities consisting of a circular cavity providing a high-$Q$ WGM that is then tunnel-coupled to a deformed cavity with a $n$-dependent composite geometry (circular arc and half of an ellipse) that guaranties robust unidirectional emission for a broad range of refractive indices from a simple resonator geometry. No phase space information is needed. We expect this simple yet efficient concept to be suitable and useful to obtain high-$Q$ modes with unidirectional emission properties in a number of future applications.

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