Imaging Molecules from Within: Ultra-fast, Ångström Scale Structure Determination of Molecules via Photoelectron Holography using Free Electron Lasers

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Abstract

A new scheme based on (i) upcoming brilliant X-ray Free Electron Laser (FEL) sources, (ii) novel energy and angular dispersive, large-area electron imagers and (iii) the well-known photoelectron holography is elaborated that provides time-dependent three-dimensional structure determination of small to medium sized molecules with Ångström spatial and femtosecond time resolution. Inducing molecular dynamics, wave-packet motion, dissociation, passage through conical intersections or isomerization by a pump pulse this motion is visualized by the X-ray FEL probe pulse launching keV photoelectrons within few femtoseconds from specific and well-defined sites, deep core levels of individual atoms, inside the molecule. On their way out the photoelectrons are diffracted generating a hologram on the detector that encodes the molecular structure at the instant of photoionization, thus providing 'femtosecond snapshot images of the molecule from within'. Detailed calculations in various approximations of increasing sophistication are presented and three-dimensional retrieval of the spatial structure of the molecule with Ångström spatial resolution is demonstrated. Due to the large photo-absorption cross sections the method extends X-ray diffraction based, time-dependent structure investigations envisioned at FELs to new classes of samples that are not accessible by any other method. Among them are dilute samples in the gas phase such as aligned, oriented or conformer selected molecules, ultra-cold ensembles and/or molecular or cluster objects containing mainly light atoms that do not scatter X-rays efficiently.

PACS numbers: 33.80.-b, 33.60.+q, 87.64.Bx
Introduction

The vision to directly follow time-dependent structural changes when molecular bonds are formed or break apart, when transition states or conical intersections are passed, namely to 'make the molecular movie' on atomic i.e. sub-nanometer length and molecular i.e. femtosecond time scales is among the strongest motivations driving huge efforts worldwide to develop next generation light sources, the Free Electron Lasers (FEL) \[1\]-\[3\]. Delivering ultra-intense bursts of $10^{13}$ coherent photons at up to 12 keV energies with pulse lengths of 10 to 100 fs and realistic prospects to reach 1 fs in the future, the 'standard' scenario is to extract the (time-dependent) structure of molecules in the gas phase via coherent X-ray diffraction. Focusing the X-rays to spots as small as 100 nm onto single objects this extends to the hope to image individual molecules in the gas phase \[6\]. This would, in principle, enable (time-dependent) structure determinations of many non-crystalizable molecules of biological interest, considered to represent a major break-through in structural biology.

Nevertheless, the realization of these visions is by far not assured essentially due to two reasons. First, even though the photon flux is huge, the tiny X-ray diffraction cross section of typically $\sim 10^{-24}$ cm$^2$ results in just a few tens to a few thousands of scattered photons in one shot from e.g. an aligned gas phase molecular ensemble or from a large, single molecule, respectively. Thus, thousands of individual shots with known relative orientation of the molecules have to be summed in order to obtain the statistical significance requested for atomic spatial resolution. Up to now there is no pathway identified without controversy to reach that goal. Second, the 'destructive' photo absorption cross section is factors of ten (e.g. for the carbon K-shell in bio-molecules) to thousand (for heavier elements) larger compared to the one for coherent diffraction of 12 keV photons causing ultra-fast delocalization of core level (via the direct photo effect) and outer-shell electrons (via the Auger effect with typical time constants of below 10 fs) culminating in the question whether the molecular structure will be first imaged and then destroyed or vice versa. Presently, common knowledge is that the maximum tolerable pulse length will be 10 fs and many investigations concentrate on the destruction issue placing e.g. scarifying layers around the object of interest \[7, 8\].

As an alternative 'table-top' method, femtosecond electron diffraction (FED) has been suggested and developed to reach the above goals on various fronts using 'conventional guns' \[9, 10\], envisioning intense laser accelerated electron bunches \[11\] or using 'rescattered' electrons in above threshold ionization \[12\]. Due to an elastic scattering cross section that is larger by about a factor of $\sim 10^6$ for 30 keV electrons compared to 12 keV photons along with the fact that inelastic, destructive reactions (electron impact excitation) occur with smaller cross sections and a factor of thousand less energy deposition compared to photon absorption, the number of electrons in the beam needed to record images as well as unwanted modifications of the sample molecules are significantly reduced \[10\]. In the most promising 'conventional gun' scenario, bunches of up to $10^5$ electrons of 30 keV within $\sim 600$ fs focused to spot sizes of 200 $\mu$m have been demonstrated to be feasible recently and structural information has been achieved. 100 fs pulse durations for bunches of $10^4$ electrons seem to be feasible optimizing existing gun designs \[10\].

Both methods, X-ray and electron diffraction have been extensively discussed and compared in literature \[10, 13\]. Drawbacks on the electron side are that it will be very challenging if not impossible to reach 100 fs time scales and below, the relatively large beam divergence and, thus, lower spatial resolution, missing coherence and, most challenging, the so-called phase match problem when extended samples (200 $\mu$m) have to be used (like molecular ensembles in the gas phase): Due to the difference in velocity between the pump photons, initiating the dynamics, and the probe electron pulse of about a factor of four (30 keV electrons), the latter needing around picoseconds for traversing the sample region, a phase-mismatch between pump and probe occurs not to be
FIG. 1: The principle of photoelectron holography (as outlined e.g. in [20]). A photoelectron p-wave is emitted from one of the atoms in the molecule via absorption of linear polarized light with photon energy $\hbar \omega$, from e.g. the K-shell of the emitter with emerging spherical wavefronts. In photoelectron holography a photoelectron diffraction pattern is viewed as an interference between that part of the photoemitted wave which propagates undisturbed into the detector, $\Psi_0$, becoming a reference wave, and the part scattered by the nearby atoms, $\Psi_s$, becoming an object wave which carries the information about the atomic positions. $\Psi_0$ and $\Psi_s$ interfere on the detector with a phase shift $\Delta \phi$ yielding thus an intensity distribution $I_p = |\Psi_0 + \Psi_s|^2$ which represents a hologram in a large portion of p-space.

overcome by shortening the pulses, essentially absent in all optical set-ups.

In this paper we present a third scheme along with model calculations, combining the best of the above-described worlds enabling us to realize the molecular movie with femtosecond time and Ångström spatial resolution for small and medium sized molecules. It relies on the availability of X-ray FELs as well as of novel high-speed read-out, energy dispersive electron imaging devices (pnCCD see e.g. [14]) and is based on the well-known photoelectron holography scenario (see e.g. [15]-[17] and references therein). Along those lines and as schematically depicted in figure 1, it is suggested to utilize the X-ray FEL pulse to produce high-energy (500 eV to 2 keV), femtosecond-pulsed and monochromatic photoelectrons in individual molecules in a gas-phase sample by exploiting the otherwise 'destructive' photo absorption effect with its large cross section. As illustrated in figure 1 emitted photoelectrons with energies specific to the atom(s) in the molecule that absorbed the photon(s) and, thus, launched at well-defined atomic sites, will on 'their way out' be diffracted on the potential of the (parent) molecule of interest with the diffraction pattern revealing, among others, the three dimensional relative Cartesian coordinates, i.e. the spatial structure of the molecule.

The method exploits the fact that photo absorption cross sections are of the order of $\sigma_{\text{photo}} \sim 10^{-20} \text{cm}^2$ at about 1 keV above an edge and, thus, typically four orders of magnitude larger than those for coherent photon scattering with $\sim 10^{-24} \text{cm}^2$ for 10 keV photons and carbon atoms. With a target line density of $\sim 10^{11} \text{molecules/cm}^2$ and a photon flux of $10^{13} \text{photons/pulse}$ one could produce up to $10^4 \text{electrons/pulse}$. Since each individual electron is created 'on the spot' with atomic spatial precision, i.e. at individual molecules, it represents a huge effective current density in the order of $10^{10} \text{A/cm}^2$ per electron on an area of $(10 \text{ Å})^2$ for an electron velocity of several $10^9 \text{cm/s}$ corresponding to keV energies and, thus, the total effective current density of $10^4 \text{electrons in the pulse reaches } \sim 10^{14} \text{A/cm}^2 \text{per pulse and } \sim 10^{16} \text{A/cm}^2 \text{per second for an FEL repetition rate of 120 Hz}. This compares with optimistic $\sim 10^8 \text{A/cm}^2 \text{per second that might be achieved in FED experiments assuming } 10^4 \text{electrons/pulse focused to a spot diameter of 200 } \mu\text{m with a pulse length of 100 fs, an electron energy of 30 keV and a gun repetition rate of 1 MHz.}$

Therefore, if combined with a large solid-angle, high-efficiency multi-hit, energy dispersive detectors, the method allows one exploring a whole class of molecules that can only be prepared as
dilute samples with densities between $10^6$ to $10^{11}$ cm$^{-3}$ as typical for aligned 18, oriented 19 or even conformer selected ensembles 20, 21, all not accessible for pump-probe structure determination by any other present techniques. Here we built on the tremendous recent development in adiabatic 18 or pulsed laser alignment (for a recent review see 22) as well as in Stark acceleration 23 techniques to manipulate and define the molecular state where an unprecedented degree of laser induced alignment and orientation has been demonstrated 19.

The present paper is aimed to provide the basic ideas and numbers for femtosecond photoelectron diffraction (FPED), illustrated using the chlorin benzene molecule and verified by simple model calculations based on the well-known concepts of photoelectron holography. We also point to the limitations of the method and develop realistic scenarios for the three-dimensional momentum imaging of the photoelectrons by exploiting fore-front pnCCD X-ray pixel cameras.

**Basic Concept and Comparison with other Methods**

In the scenario illustrated in figure 1 we produce the photoelectron inside of an individual molecule in the sample with femtosecond time and $\sim 10^{-3} - 10^{-4}$ relative energy resolution, ultimately limited by the FEL radiation properties (here, seeded beams are envisioned for the future with 1 fs or even sub-fs time-resolution). On its way out the photoelectron wave, launched at one specific atom of the molecule (emitter) is partly diffracted on the individual atoms of the parent molecule (scatterers), as depicted in figure 1 for the most simple situation of only one scatterer, or reaches the detector directly, representing a reference wave for the scattered part. As described in 16 the electron wave with wavelength $\lambda$ is fully coherent over a length of $l_c = \lambda^2/\Delta \lambda$, i.e. over distances of $\sim 10$ nm to $\sim 0.1$ nm in the worst case, safely across medium-sized molecules, for an energy uncertainty of the FEL beam of $\Delta E_\gamma/E_\gamma \sim 10^{-4}$ at a few keV, translating in an uncertainty of the photoelectron energy of $\Delta E_e/E_e \sim 10^{-3} - 10^{-4}$. Thus, a hologram is generated at the detector and, if the diffraction pattern is recorded over a large part of the solid angle, it allows one an immediate interpretation for photoelectron energies beyond $\sim 500$ eV.

At the same time we transfer the nm wavelength of 1 keV to 10 keV photons to an to electron deBroglie wavelength $\lambda_e = h/\sqrt{2m_e E_e}$ between $\sim 0.6$ Å to 0.3 Å for $E_e = 500$ eV or $E_e = 2$ keV photoelectrons, respectively, allowing us to achieve Ångström spatial resolution as demonstrated recently 17.

In order to retrieve the structure of the molecule from the hologram on the detector three-dimensional electron momentum $P_e = (p_x, p_y, p_z)$ images have to be recorded covering a large part of the final momentum space. This is achieved with an energy dispersive pixel pnCCD detector as described later, determining two momentum components from the electron hitting position on the detector and the third one from the measured energy of the photoelectron $E_e = \hbar \omega - I_{n,l}$ via energy-momentum conservation relations ($\hbar \omega$ is the photon energy and $I_{n,l}$ is the binding energy of the atomic $n, l$ shell that is photo ionized). Electrons are emitted from molecules that are aligned, oriented or conformer selected by methods 18-23 described in some detail later.

The method as proposed here comprises several new concepts, builds on fore-front technologies in various areas and combines them in a unique way:

(i) Exploiting the new FEL light sources delivering intense ($10^{13}$ photons per pulse), short-time ($\sim 100$ fs with prospects of achieving 1 fs or even below) and coherent VUV or X-ray pulses with energies of 100 eV < $\hbar \omega \gamma$ < 12 keV 1-5.

(ii) Building on the ability to align, orient or conformer select in three dimensional space the molecules of interest with major progress achieved in the recent past 18-23.

(iii) Using high-energy electrons ($500$ eV < $E_e$ < 2 keV) for diffraction where the patterns are much simpler for interpretation in terms of photoelectron holography 15-17, 24-25.
(iv) Applying a new concept for 3D electron momentum imaging based on recently developed, large area, energy and position dispersive, single electron counting pnCCD detector devices [14].

(v) Creating the photoelectrons directly by the X-ray pulse we do have an effective 'all optical approach' in pump-probe experiments, thus, not facing the phase matching problem as in FED measurements using conventional electron guns [10].

Thus, our method represents a major step forward compared to all previous concepts as e.g. so called molecular frame photoelectron angular distribution (MFPAD) spectroscopy being now a standard technology at synchrotron radiation facilities. Based on a recent experimental breakthrough in angle-resolved photoelectron-photoion coincidence techniques [26]-[28], culminating in using reaction microscopes (REMI) [29]-[35] that allow one for the coincident detection of the 3D vector momenta of several electrons and ions, low-energy photoelectron angular distributions from free, 'fixed-in-space' molecules are recorded. Here, in present experiments, the molecular orientation is retrieved a posteriori via coincident detection of heavy molecular fragments making this method extremely demanding technologically and limiting it to essentially diatomic molecules where, in addition, the axial recoil approximation has to hold. Since (multi-) coincidences are requested, typically less then one event per beam pulse can be accepted for a reliable analysis of the data, thus requiring MHz repetition rates from the pulsed radiation source as available at synchrotrons in order to take multi-dimensional data with sufficient statistical significance. Moreover, due to the timing properties of synchrotrons in the range of 100 ps, no short-time pump-probe experiments can be realized. Femtosecond slicing devices available at some synchrotrons do not deliver enough photons for such investigations [36]. Finally, only low-energy electrons $E_e < 50$ eV have been recorded up to now (manly due to the time-of flight spectroscopy methods used) that makes the interpretation of the data demanding. Nevertheless, scattering patterns provided detailed information to an unprecedented level about a variety of processes such as localization of charges [32] and core holes [33], interferences in molecular double-slit or multi-slit arrangements [34], phases of photoelectron waves [38, 39], and, last but not least, the electronic potentials and the molecular structure via photoelectron diffraction [35, 40].

It also decisively extends the huge area of previous ultra-fast pump-probe, 'femto-chemistry' studies (see e.g. [41]) performed with long-wavelength (optical) probe lasers that can only indirectly deliver final-state (time of probe) structure information of smaller molecules based on spectroscopic knowledge of the potential curves accessed by the probe pulse. Since the potential curves along the reaction coordinate usually cannot be calculated for larger molecules, this method remained limited to smaller species.

Reaching femtosecond timescales without the need of crystallization of samples we can access a different class of molecules as well as ultra-short times, well below the picosecond time-resolved experiments recently performed at synchrotrons (see e.g. [42]).

Last but not least our method is expected to have certain advantages compared to using VUV high-harmonic radiation as a probe pulse and which has already lead to first successful measurements (see e.g. [43]). In the latter, up to now, photons are not high-energetic enough at acceptable intensities to access core-level electrons and, thus, to specify in details the birth location of the photoelectron. Since in principle, attosecond time resolution can be achieved with this technology both methods might be considered as complementary.
Theoretical Description and Results

Let us consider the photo ionization of a molecule assuming that this process can be regarded as an effectively single-electron problem. The corresponding Schrödinger equation reads

$$i \frac{\partial \Psi}{\partial t} = \left( \hat{H}_0 + \hat{W}_{EM}(t) \right) \Psi.$$ \hspace{1cm} (1)

Here, $\Psi = \Psi(\mathbf{r}, t)$ is the electron wave function which is space and time dependent and describes the dynamics of the ‘active’ electron in the photo ionization process. Further, $\hat{H}_0$ is the Hamiltonian for the electron in the absence of the electromagnetic field and

$$\hat{W}_{EM}(t) = \mathbf{A} \cdot \hat{\mathbf{p}} / c \hspace{1cm} (2)$$

is the interaction between the electron and the field, where $\hat{\mathbf{p}}$ is the operator for the electron momentum, $\mathbf{A}$ is the vector potential of the field and $c$ is the speed of light. Assuming that the field is linearly polarized we take

$$\mathbf{A}(\mathbf{r}, t) = A_0 \cos(\omega_0 t - \mathbf{k}_0 \cdot \mathbf{r}). \hspace{1cm} (3)$$

Here $\mathbf{r}$ and $t$ are the space and time coordinates, $\omega_0$ and $\mathbf{k}_0$ are the frequency and wave vector and $A_0 = a_0 e$, where $e$ is the polarization vector ($e \cdot \mathbf{k}_0 = 0$) and $a_0 = c F_0 / \omega_0$ is the amplitude of the vector potential with $F_0$ being the strength of the electromagnetic field.

Below we shall discuss two approaches to address photo ionization. In one of them the process is dealt with by finding the wave function, which is a solution of Eq. (1) satisfying appropriate initial and boundary conditions and which describes the evolution of the electron wave packet in time and space. The second approach, which does not consider the space-time characteristics of the process, is based on obtaining the transition amplitude which enables one to calculate the momentum spectrum of the emitted photoelectrons. Clearly, these two approaches can be considered as complementary.

Approach 1

The wave function $\Psi = \Psi(\mathbf{r}, t)$ can be expanded according to

$$\Psi(t) = g(t) \psi_i(t) + \int d^3 \mathbf{p} \beta_\mathbf{p}(t) \psi^{(+)}_\mathbf{p}(t), \hspace{1cm} (4)$$

where $\psi_i(t)$ and $\psi^{(+)}_\mathbf{p}(t)$ are solutions of the field-free Hamiltonian

$$i \frac{\partial \psi}{\partial t} = \hat{H}_0 \psi, \hspace{1cm} (5)$$

for bound and continuum states of the electron, respectively, and $g(t)$ and $\beta_\mathbf{p}(t)$ are the time-dependent expansion coefficients.

Since in the (tightly) bound state the electron is very well localized we can approximate $\psi_i(t)$ as

$$\psi_i(t) = \varphi_i(\mathbf{r} - \mathbf{R}_0) \exp(-i \varepsilon_0 t), \hspace{1cm} (6)$$

where $\varphi_i$ is the state of the electron bound in the atom, whose nucleus has the coordinates $\mathbf{R}_0$, and $\varepsilon_0$ is the corresponding binding energy.
In order to build states $\psi_p^{(+)}(t)$ representing the stationary continuum spectrum we shall assume that the kinetic energy of the electron motion in the continuum is sufficiently high and, therefore, $\psi_p^{(+)}(t)$ can be obtained in the first order approximation in the interaction between the electron and the atomic centers constituting the molecule. This yields

$$
\psi_p^{(+)}(t) = \frac{\exp(-iE_pt)}{(2\pi)^{3/2}} \times \left( \exp(ip \cdot r) + \frac{1}{(2\pi)^{3/2}} \sum_j \exp(i(p \cdot R_j)) \int d^3p' \tilde{V}_j(p' - p) \exp(i(p' \cdot (r - R_j))) \right) \tag{7}
$$

Here $p$ and $E_p = p^2/2m_e$ ($p = |p|$) are the momentum and energy, respectively, of the continuum state and

$$
\tilde{V}_j(q) = \frac{1}{(2\pi)^{3/2}} \int d^3r V_j(r) \exp(-iq \cdot r) \tag{8}
$$

is the Fourier transform of the interaction $V_j(r) = V_j(r - R_j)$ between the electron and the $j$-th atomic center of the molecule whose nucleus is located at a point with the coordinates $R_j$. In Eq. (7) $\alpha \to +0$ shows how to handle the singularity and the sum runs over all atomic centers of the molecule, $j = 0, 1, ..., N - 1$ where $N$ is the number of atoms, including the emitting one $(j = 0)$. One should note that in (7) we have neglected all inelastic channels corresponding to energy transfers between the emitted photoelectron and the internal degrees of freedom of the residual molecular ion. Note also that the state (7) is the so called 'out-state', which asymptotically (at large distances between the electron and the residual molecule) is a superposition of a plane and an outgoing scattered wave.

In order to obtain the unknown coefficients $g(t)$ and $\beta_p(t)$ we insert the wave function (4) into the Schrödinger equation (1) and use the rotating-wave approximation. This leads to the following system of differential equations

$$
i\frac{dg(t)}{dt} = \int d^3p W_{g,p} \exp(i\omega_0 t)\beta_p(t)
$$

$$
\begin{align*}
i\frac{d\beta_p(t)}{dt} &= W_{g,p}^* \exp(i\omega_0 t)g(t),
\end{align*}
$$

where

$$
W_{g,p} = \frac{1}{2e} \int d^3r \psi_0^*(t = 0) \exp(-ik \cdot r)(A_0 \cdot \hat{p})\psi_p^{(+)}(t = 0). \tag{10}
$$

Assuming for the moment that the electromagnetic field is suddenly switched on at $t = 0$, when the electron was in the state $\psi_i$, the initial conditions for the system (9) are given by $g(t = 0) = 1$ and $\beta_p(t = 0) = 0$.

Here we shall not go in details of how the system (9) can be solved and the state (11) derived and merely note that one can show that at asymptotically large distances between the photoelectron and the residual molecule the wave function $\Psi(t)$ can be presented in the following approximate form

$$
\Psi(r, t) = \exp(-iE_e t) \times \left( \frac{\exp(ip \xi_0)}{\xi_0} \exp(-\Gamma(t - \xi_0/v_e)) \theta(t - \xi_0/v_e) \right)
$$

$$
\times \sum_{l=0}^{\infty} \sum_{m=-l}^{+l} B(l, m; l, m; \xi_0/\xi_0) +
$$
\[
\sum_{j \neq 0} \exp(i p_e \xi_j) \exp(i p_e R_{j0}) \frac{\exp(-\Gamma(t - (\xi_j + R_{j0})/v_e))\theta(t - (\xi_j + R_{j0})/v_e)}{R_{j0}} \times \sum_{L=0}^{+L} \sum_{M=-L}^{\infty} \sum_{l=1}^{\infty} C(l_i, m_i; L, M; l, m; \xi_j/\xi_0, R_{j0}/R_{j0}) \right). 
\]

(11)

Here, \(E_e = \varepsilon_0 + \omega_0\) is the energy of the emitted electron, \(\Gamma (\Gamma \ll E_e)\) is the half-width of the initial electron state caused by the photo effect, \(p_e = \sqrt{2m_e E_e}\) and \(v_e = p_e/m_e\) are the absolute values of the electron momentum and velocity, respectively, \(\xi_j = r - R_j, R_{j0} = R_j - R_0, l_i\) and \(m_i\) are the angular momentum and its projection in the initial electron state \(\psi_i\) and \(\theta\) is the (stepwise) theta-function. The functions \(B(l_i, m_i; l, m; \xi_0/\xi_0)\) and \(C(l_i, m_i; L, M; l, m; \xi_j/\xi_0, R_{j0}/R_{j0})\) have rather complicated forms and will be specified elsewhere.

The physical meaning of the state Eq. (11) is rather transparent. This state describes an electron wave packet which is a superposition of the wave, propagating directly from the initial electron location (the first two lines in the parentheses), and of the 'secondary' waves, appearing due to the electron scattering on all other atomic centers in the molecule (the last two lines). The theta-functions in Eq. (11) emphasize the fact that in order to traverse a distance \(L\) an electron moving with a velocity \(v_e\) needs the time \(L/v_e\) and the decaying exponential factors reflect the depletion of the electron population in the initial state due to the emission.

**Approach 2**

The spectrum of photoelectrons emitted from the molecule can be calculated using the transition amplitude

\[
S_{fi} = -i \int_{-\infty}^{+\infty} dt \langle \psi_f(t) | \hat{W}_{EM} | \psi_i(t) \rangle.
\]

(12)

where \(\psi_i(t)\) is given by Eq. (11) and \(\psi_f(t)\) is the so called 'in-state' for the emitted electron, \(\psi_f(t) = \psi_{p}^{(-)}(t)\), which is obtained from the 'out-state' \(\psi_{p}^{(+)}(t)\) according to \(\psi_{p}^{(-)}(t) = (\psi_{p}^{(+)}(t))^*\). Inserting the states \(\psi_i(t)\) and \(\psi_{p}^{(-)}(t)\) into (12) and integrating over the time and space coordinates we obtain

\[
S_{fi} = -\frac{\pi i}{c} \exp(i k \cdot R_0) G_{fi} \times \delta (E_p - \varepsilon_0 - \omega_0),
\]

(13)

where

\[
G_{fi} = (A_0 \cdot p) \bar{\varphi_i}(p - k) \exp(-i p \cdot R_0) + \frac{1}{(2\pi)^{3/2}} \sum_j \exp(-i p \cdot R_j)
\]

\[
\times \int d^3 p' \frac{\bar{V}_j (p - p')}{E_p - E_{p'} + i\alpha} \exp(i p' \cdot (R_j - R_0))(A_0 \cdot p') \bar{\varphi_i}(p' - k).
\]

(14)

The \(\delta\)-function in (13) expresses the energy conservation in the photo effect and

\[
\bar{\varphi}(q) = \frac{1}{(2\pi)^{3/2}} \int d^3 r \varphi(r) \exp(-i q \cdot r)
\]

(15)

is the Fourier transform of the initial electron state.

Using the standard consideration for finding the momentum distribution of the photoelectrons from the transition amplitude we obtain that this distribution is given by

\[
\frac{d\sigma}{d^3 p} = \frac{\pi}{2\varepsilon_c^2} |G_{fi}|^2 \times \delta (E_p - \varepsilon_0 - \omega_0).
\]

(16)
The knowledge of the momentum distribution of the emitted electrons and the experimental geometry enables one to calculate the electron intensity on the detector.

Results

In the present paper we will not present results obtained with the wave function (11). Instead, assuming that $\Gamma \rightarrow 0$ and considering only the space-time points with $v_e t > \xi_j + R_{j0}$, we shall replace expression (11) by a simpler one which was earlier used in the studies of inside photoelectron holographic imaging of solids [15]-[17].

We take the principle scenario depicted in figure 1 and consider the photo ionization of a chlorine molecule (see figure 2) from the $K$-shell of the Cl atom by a beam of 4.5 keV FEL photons. The photons are assumed to be linearly polarized along the $y$-axis in the case of geometry I (figure 3) and along the $z$-axis in the case of geometry II (figure 11). The photon absorption results in the emission of a 1.7 keV electron which scatters on the carbon atoms of the molecule before reaching the detector (we neglect the hydrogen atoms as scatterers because of their relatively weak field).

A monochromatic electron source $p$-wave $\Psi_{source}$ is launched from the $K$-shell of Cl by dipole transition

$$\Psi_{source} = A \frac{\exp(ip_e \xi_0)}{\xi_0} Q_1(\xi_0) Y_{1,0}(\xi_0/\xi_0)$$

with the radial part $Q_1$ and spherical harmonic $Y_{1,0}$ describing the electron preferably ejected along the electric field vector.

In the single scattering picture, the total wave $\Psi_{tot}$ on the detector plane is

$$\Psi_{tot} = \Psi_{source}(\xi_0) + \sum_j f_j(\Theta_j) \frac{\exp(ip_e \xi_j)}{\xi_j} \Psi_{source}(\xi_0 - \xi_j).$$

Here $\Theta_j$ is the scattering angle and $f_j(\Theta_j)$ the scattering amplitude, which in the first Born approximation is given by

$$f_j(\Theta) = -\frac{m_e}{2\pi \hbar^2} \int d^3 \xi V_j(\xi) \exp(-i \mathbf{q} \cdot \xi),$$

where $|\mathbf{q}| = 2p_e \sin(\Theta/2)$. The simple expression (18) should be a reasonable approximation if the size of the space, where the scattering potential $V_j$ is effectively located, is substantially less than the distance $R_{j0}$. The Born approximation is safely valid for $\sim 1$ keV photoelectrons.
In a first step we take geometry I sketched in figure 3 and only consider two out of the six carbon atoms of the molecule which are marked in figure 3 by solid circles. The calculated hologram \( I(p_x, p_z) = |\Psi_{tot}|^2 \) is shown in figure 3. The hologram \( I(p_x, p_z) \) can be inverted by mathematical means to yield real space images that locate individual atoms surrounding the emitter. Here we adopt a reconstruction formalism based on the Helmholtz-Kirchoff integral theorem as proposed in [44], where the amplitude of the object wave field at any point \( r \) in space near the emitter can be calculated by Fourier transforming phased two-dimensional photoelectron hologram. In principle it should be possible to achieve a sub-Ångström spatial resolution \( \delta r \propto \pi/p_e \), however the anisotropy of the electron scattering (with forward scattering being a major obstacle) produces artifacts in the reconstructed images which are manifested as a small distortions and peak shifts from the real space images amounting about 1 Å. Several procedures to correct these effects and thus to improve the image quality and/or extract additional informations have been proposed: some of them are based on the inversion formalism [45], [17] whereas others exploit small changes in diffraction condition (see, for example, [24]).

Next we assume geometry II sketched in figure 6 and consider now all six carbon atoms as scatterers. In this case we obtain an interference hologram shown in figure 7. Retrieval of the structure yields several spots at the positions of the carbon nuclei as well as their mirror images (see figure 8).
FIG. 5: Atomic images in the plane x-z, 6 Å above the emitter, reconstructed from the hologram shown in figure 4. As usual with inside-source holography, the emitter (indicated by a circle) sits at the origin of the image and is not reproduced.

FIG. 6: A sketch of geometry II showing the emitter (Cl atom) which is taken as the origin of the coordinate system and six scatterers (C atoms) on the $x_0 - z_0$ plane.

Note also that we have performed calculations for the system and geometries using the approach 2. We have found that, compared to the description discussed above, these calculations lead to holograms, which possess the same qualitative features (see for instance figure 9) and, thus, yield the same molecular structure.

Summarizing the above brief discussion we can conclude that our quantum calculations, that should be sufficiently accurate at this high photon energy, reveal the salient interference features due to the scattering of the outgoing photoelectron from the different atoms in the molecule and, thus, support the basic idea brought forward in this paper.

Possible technical realization using chlorine benzene as a model system

**Radiation source:** LCLS provides $N_\gamma \sim 10^{13}$ photons at up to 10 keV in 75 fs pulses at a design repetition rate of 120 Hz which will be the basis of our estimates. We assume to focus the radiation to a spot diameter of 10 μm. Recently, lasing at 8.3 keV has been demonstrated with a $10^{12}$ photons per pulse at a width of 75 fs and beam-time will be allocated in late 2010 at the XPP endstation.
FIG. 7: The calculated photoelectron hologram for geometry II. Here a 1.7 keV photoelectron emitted from the Cl atom is scattered by six C atoms located on the $x_0$-$z_0$ plane.

FIG. 8: Positions of the scatterers (and the mirror image) 1 Å above the emitter retrieved from the hologram shown in Fig. 7.

**Aligned target**: Rotationally cold molecules can be delivered by a supersonic jet using a pulsed Even-Lavie nozzle [46, 47]. Intersecting the cold molecular jet in the interaction region with pulses from a seeded, nanosecond Nd:YAG alignment laser, synchronized to the LCLS pulses yields adiabatic 1$D$ and 2$D$ alignment of the molecular samples in space. Orientation of molecules in 1$D$ or 2$D$, the latter meaning that the molecule is controlled in all three spatial dimensions can be achieved using mixed laser and dc electric fields. Adopting the numbers put forward in one of the proposals to LCLS on coherent diffraction imaging on adiabatically aligned dibromo benzene, densities up to $10^{11}$ cm$^{-3}$ 2$D$ aligned chlorine benzene molecules can be achieved resulting in a target line density of $\Delta x = 10^{10}$ cm$^{-2}$ assuming a target that is 0.1 cm extended along the FEL beam direction which will be the basis of the present estimates. Applying additional fields for orienting the molecules or even obtaining conformer selected samples significantly decreases the target densities to values that might be as small as $10^6$ cm$^{-3}$.

**Photoelectron energies and absorption cross sections**: Photon absorption can take place in any electronic state of the molecule with strongly varying cross sections. Large values are achieved close to edges, where the photon energy matches the binding energy of the respective electron resulting in typical cross sections of $\sim 10^{-18}$ cm$^2$ and producing low-energy photoelectrons. Above the edge, the cross section for that specific shell decreases rapidly with about $(\hbar \omega \gamma)^{-3.5}$. Assuming that core-level electrons of the atomic constituents of the molecule are essentially char-
acterized by their atomic energy levels and cross sections we adopt one situation in which 4.5 keV photons irradiate the molecules. In such a case the dominant channel of the electron emission is photon absorption by the $K$-shell electrons of Cl with the cross section of $\sim 10^{-20}$ cm$^2$. The other absorption channels are not only much weaker but also lead to the emission of electrons having much higher energies. Therefore, they can be easily separated from the main channel and in what follows will simply be ignored.

**Numbers of emitted photoelectrons:** Assuming an electron detection efficiency of one we can estimate the number of recorded photoelectrons per pulse according to $N_{pe} = \Delta x \sigma_{photo} N_\gamma$ ending up with about $N_{pe}(\text{Cl}\,K) \sim 10^3$. With a repetition rate of 120 Hz the corresponding rate would be $1.2 \times 10^5$ electrons per seconds. In order to estimate the time required to record a snapshot of the molecular structure one needs in addition the elastic scattering cross section for the interaction of the launched photoelectrons with the atoms in the molecule on their way out which is implicitly included in our later theoretical simulations. Taking into account the p-wave character of the emitted photoelectrons and assuming that each of them interacts with its parent molecule only, the count rate, which in addition depends on the relative orientation of the molecule with respect to the (dipolar) photoelectron emission characteristics and the position of the detector, will be between 5000 electrons/s and 60000 electrons/s. Assuming 300000 electrons to be detected in order to obtain structural information of a medium sized molecule at a certain time delay between pump and probe pulses, a full image might be recorded in a matter of seconds to few minutes for one time step.

From these considerations it is obvious that ultra-dilute samples with line densities as small as $10^6$ cm$^{-2}$ like for conformer selected molecules only become accessible at photon energies slightly above one of the edges of the atomic constituents of the molecule exhibiting cross sections on the order of $10^{-18}$ cm$^2$ and photoelectron energies of not more than 100 eV. Nevertheless, assuming the full performance of the LCLS with repetition rates as high as 120 Hz we still end up with about 10-120 photoelectrons per second such that a measurement of the structure, again requesting about 300000 events would take about two to ten hours.

From these considerations it becomes also obvious that direct coherent X-ray diffraction of oriented or even conformer selected molecules with elastic photon scattering cross sections of the order of $10^{-24}$ cm$^2$ are completely unrealistic! The same holds for FED where in the most optimistic case $10^4$ electrons in 100 fs pulses might hit the target at 1 MHz repetition rate. With elastic scattering cross sections on the order of $10^{-19}$ cm$^2$ and a target line density of $10^6$ molecules/cm$^2$ this yields a few scattered electrons per hour.
FIG. 10: Geometry for high-energy electron detection with the pnCCD in CAMP.

Thus, the technology presented here does indeed allow one to access a large number of samples that are of fundamental and benchmarking interest for tracing molecular dynamics during chemical reactions. For lower photoelectron energies, not considered in this article but as used presently at synchrotrons in similar, time-independent experiments the speed for taking structural images would be limited by the count rates accepted by the various detectors as well as by space charge effects blurring the image forcing one to reduce the incoming flux.

Energy Dispersive Large-Area Electron Momentum Imaging.

The new method for obtaining structural information of atomic positions with Ångström resolution in molecules as a function of time via femtosecond holographic imaging of photoelectrons relies, apart from the availability of X-ray FELs and of 2D oriented molecular samples, decisively on high-speed, large-solid-angle, energy-dispersed, quasi-continuous along two spatial dimensions and highly efficient detection of high-energy electrons. This can be achieved, for the first time, by new solid-state pnCCD cameras, originally developed for X-ray detection at FELs and implemented into the CFEL-ASG-Multi-Purpose (CAMP) chamber developed by the Max-Planck Advanced Study Group (ASG) at the Center for Free Electron Laser science (CFEL) in Hamburg. The chamber along with the detectors have been described in detail before [14] such that we will concentrate on the salient features and specific requirements to be fulfilled for electron detection.

Due to the pixel size of 75 µm × 75 µm over a total area of 8 cm × 8 cm we can image the electrons in a quasi-continuous way along two spatial dimensions covering a large solid angle as requested. The high granularity of the detector simultaneously ensures, that large numbers of electrons, certainly 10⁴ per shot, can be recorded in an energy dispersed way which is feasible as long as each of the 10⁶ pixels is hit by not more than one electron. Moreover, the unprecedentedly high frame read-out rate of up to 200 Hz is adapted to the maximum FEL repetition rate at LCLS of 120 Hz, such that electrons can be recorded shot-by-shot.

More care has to be taken concerning the energy resolution of the detector which is excellent, close to the theoretical limit (one-electron noise) for X-ray detection. Electrons, however, have to penetrate through a protecting (50 nm Al) as well a charge carrier, isolating depletion layer (40 nm SiO₂) meaning that only electrons at around 10 keV can be detected with a probability of close to one and reasonable energy resolution, limited by the energy loss of the electrons in the entrance layers. Thus, electrons of 500 eV to 2 keV as considered to be ideal for the present purpose cannot be directly monitored but, rather, have to be post-accelerated towards the detector.

For that purpose, a potential grid on a voltage of 10 kV will be placed about 1 cm away from the interaction zone as depicted in figure [10] allowing to accept a solid angle ΔΩ/2π ≈ 0.74 with the pnCCD (8 cm × 8 cm) as close as 2 cm downstream of the grid. Thus, the potential grid,
FIG. 11: Response of the pnCCD on electrons of different energies as indicated penetrating 40 nm SiO$_2$ insulating and 50 nm Al laser-light protection layers.

Serving for enhancing the solid angle, at the same time post-accelerates the electrons to 10.5 keV or 12 keV, respectively, enabling them to penetrate into the pnCCD through various protecting and carrier depletion layers. They are then detected with a FWHM of about 500 eV as demonstrated in a recent test measurement shown in figure 11 for electrons of different energies emerging from a electron microscope directly hitting (zero degree impact) the pnCCD. Thus, electrons with energies of around 1.7 or 3.5 keV emitted simultaneously in the present situation will end up with final energies of 11.7 keV or 13.5 keV, respectively, and, thus, can be easily discriminated against each other. In practice, that means that one can, in properly chosen situations, obtain holographic images simultaneously taken at two (several) photoelectron energies, illuminating the molecule from different sites from within. On the other hand, the electron energy resolution of 500 eV clearly limits the method to cases where the photoelectrons emerging from different atoms in the molecule can be cleanly separated. Ideal cases are emitters with atomic numbers between chlorine ($Z = 17$) to gallium ($Z = 31$) as constituents of organic molecules containing essentially light atoms with $Z < 10$ with their K-shell energies (Cl: 2.8 keV to Ga: 10.4 keV) clearly separated from those of the lighter constituent atoms (C: 0.28 keV, H: 0.014 keV, up to F: 0.7 keV) as well as from photoelectrons emerging from the L- and M-shells of the heavy species. Thus, even though the situation is not completely ideal, the large selection of constituent atoms for launching electrons from within allows one to certainly choose benchmark situations for chemical dynamics. Prominent examples are all (poly) pentene rings containing one Cl atom, easily attachable at different sites as emitter. Other molecules of interest for performing benchmarking, photoionization or dissociation experiments might be clorethyle [49] or diphenylmethyl chloride [50].

**Summary and Outlook**

We have developed a novel idea and provided model calculations for 'imaging molecules from within', which exploit the holographic diffraction pattern occurring when photoelectrons, site-specifically launched at certain atoms within molecules, are scattered off the three dimensional molecular potential on their way out. The observed patterns encode the 3D molecular pattern which is retrieved with Ångström resolution using reconstruction algorithms that have been developed for 'inside photoelectron holography' in solid state physics. Since femtosecond pulsed photon beams from X-ray free electron lasers are used to create the photoelectrons, the structure determi-
nation proceeds on an ultra-fast time scale. Along with the large number of photoelectrons that are produced due the high intensity of the FEL radiation, they are perfectly suited for probing the time-dependent structure of the object under investigation in pump-probe arrangements where the dynamics is induced either by an optical pump laser or by a replica of the FEL pulse itself as recently demonstrated at the FLASH [51].

Different from any other scenario for coherent structure determination, we measure the three-dimensional momentum vectors of high-energy electrons \(E_e > 500\, \text{eV}\) with large solid angle and energy dispersed exploiting recently developed large-area pnCCD detectors along with an electric field projection technique. Along with the unique short pulse properties of the FEL, this represents the ultimate technology to obtain real-time 3D structural information for small to moderate-size molecules by providing several unique features:

(i) As the outgoing electrons are diffracted in the combined electronic and nuclear charge distribution of the molecule, the diffraction pattern does not 'only' reveal information on the position of the nuclei but, moreover, on the complete multi-center molecular potential, i.e., the electronic orbitals. This is especially obvious when low-energy electrons are used to create the diffraction pattern. Thus, investigating the same reaction using photoelectrons of different energies, readily adjustable via tuning the FEL photon energies, it is expected (by comparison of the holographic images) to directly access the subtle interplay between electronic orbital and nuclear position dynamics beyond the Born-Oppenheimer approximation.

(ii) By changing the photon energy and, thus, the energy and the de Broglie wavelength of the emerging electron, the latter can be 'adjusted' to any length-scale of interest for the respective molecule, possibly even to large-scale structures such as the folding patterns of proteins, in an 'inside-source holography' arrangement. Especially for larger proteins, it might, at some point, not be important to determine the position of each individual atom but, rather, to monitor the motion of groups of atoms with a 'fixed' structure relative to other groups.

(iii) Using high-energy photoelectron holography, it was demonstrated in solid state physics, that the positions of up to around 50 nearest neighbor atoms could be retrieved. Even though this seems not to be really much if the dynamics in a large molecule e.g. a protein shall be explored, it might be an ideal method to trace the decisive early-time dynamics around a photo receptor site.

(iv) While pump-probe experiments that study the time-dependent evolution of molecular valence orbitals have recently been performed with high-harmonic laser sources [43], our approach using shorter wavelength probe pulses allows accessing localized inner-shell electrons, which is essential for structural determination via electron diffraction since it allows launching the photoelectron from specific sites within the molecule.

(v) Due to the possibility to simultaneously measure both ions and high-energy electrons in CAMP, we will be able to continuously monitor the degree of alignment as well as the fragmentation channels (via measuring the fragment kinetic energies) in the pump-probe experiments while taking the electron diffraction data. This \(\text{(quasi-)}\) coincidence mode may also allow cleaning up the experimental data in the post-analysis, especially if covariant mapping methods [52] are applied.

(vi) Since the core-holes created as a consequence of photoelectron emission decay either via emission of Auger electrons or of fluorescence photons, it should be possible (if the various energies can be separated in the pnCCD) to also record holographic images for these reaction products, as demonstrated as well in solid state physics. Auger decays typically take place on a time-scale of about 10 fs, i.e. within the present FEL pulse length, and may, in certain cases, directly influence the photoelectron emission. Radiative transitions in medium heavy atoms on the other hand are one to two orders of magnitude slower and, accordingly, would not affect the angular distribution of the directly emitted photoelectron.

(vii) Since the intensities required for the X-ray probe pulse are rather small (large focal diameters) compared to X-ray diffraction studies (due to the fact that photoionization cross sections
close to an edge are several orders of magnitude larger than X-ray scattering cross sections), radiation damage during the pulse is negligible. Furthermore, this makes photoelectron diffraction a viable tool to study ultra-thin ensembles, such as beams of conformer-selected molecules, Stark decelerated (trapped) molecules with typical target densities of only about $10^6$ cm$^{-3}$ or ultra-cold (molecular) ensembles in Bose-Einstein condensates or degenerate Fermi gases. To the best of our knowledge, structural dynamics of this rather large class of samples will not be accessible by any other present technique.

Acknowledgement

Support from the Max-Planck Advanced Study Group at CEFL is gratefully acknowledged. BN would like to thank DFG for support under the project VO 1278/2-1. We would like to thank Sascha Epp, Artem Rudenko, Simone Tecrert, Robert Moshammer, Ilme Schlichting, Robert Hartmann, Regine de Vivie-Riedle and Henrik Stapelfeldt for helpful discussions.

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