We study the dynamics and phase behaviour of a dry suspension of microtubules and molecular motors. We obtain a set of continuum equations by rigorously coarse graining a microscopic model where motor-induced interactions lead to parallel or antiparallel ordering. Through numerical simulations, we show that this model generically creates either stable stripes, or a never-settling pattern where stripes periodically form, rotate and then split up. We derive a minimal model which displays the same instability as the full model, and clarifies the underlying physical mechanism. The necessary ingredients are an extensile flux arising from microtubule sliding and an interfacial torque favouring ordering along density gradients. We argue that our minimal model unifies various previous observations of chaotic behaviour in dry active matter into a general universality class.

Recent studies of active matter, comprising particles that convert internal energy to relative motion – exerting force or torque dipoles on the surrounding medium as they do so – reveal that these systems generally function far from equilibrium and possess no passive analogues. Instead, their microscopic models can sometimes be grouped into unique “universality” classes, and identifying the corresponding continuous equations is currently an area of active research. For systems with orientational order (i.e., active liquid crystals), two important classes of models that emerged in the process are momentum-conserving (“wet”) incompressible systems, and non-momentum conserving (“dry”) compressible ones, with the vast majority of work dedicated to the former class.

Here we propose a new universality class of dry active systems defined by the following continuum equations:

\[
\frac{\partial \rho}{\partial t} = \nabla^2 \left[ \frac{1}{32} \rho + \mu \rho^2 \right] + \delta_i \partial_j \left[ \frac{\pi}{48} + \chi \rho \right] Q_{ij} - \lambda \nabla^2 (Q_{li} Q_{li}),
\]

\[
\delta_i Q_{ij} = \left[ 4 \left( \frac{\rho}{\rho_{rr}} - 1 \right) - \alpha Q_{li} Q_{li} + \kappa \nabla^2 \right] Q_{ij} + \zeta D_i \rho - \beta_1 D_i (Q_{li} Q_{li}) - \beta_2 Q_{li} D_i Q_{li},
\]

where a tensorial field \( Q_{ij} \) quantifies the nematic (apolar) ordering of the active particles, and \( \rho \) is their density; \( i, j = \{x, y\} \) denote the two-dimensional Cartesian components, and \( D_i = \partial_i - (1/2) \partial_j \partial_j \partial_i \). We demonstrate that these equations arise naturally from a microscopic kinetic theory of model mixtures of microtubules (MTs) and molecular motors (MMs). While wet incompressible active gels are generically unstable to orientational fluctuations ultimately resulting in “active turbulence”, we show that compressible dry MT-MM mixtures undergo seemingly similar chaotic dynamics, which we name dry active turbulence. The underlying mechanism is, however, completely different and we use Eqs. (1) and (2) to elucidate it: importantly, in our case concentration inhomogeneities play a central role. We note that similar dynamical patterns were observed, mainly at the level of a kinetic theory, for a very different physical system, a suspension of flocking self-propelled particles with nematic alignment. We therefore argue that dry active turbulence unifies various previous observations of chaotic behaviour in nematically ordered
microtubules and flocking self-propelled particles.

Here, we consider the dynamics of pattern formation in model MT-MM mixtures that have actively been studied as biological and synthetic instances of active matter \cite{21,22,23,24,25}. On the one hand, they incorporate the essential ingredients of the mitotic spindle \cite{23,24,25}, on the other hand, they closely mirror the so-called “hierarchical active matter”, which can be self-assembled in the lab from MTs and MMs, in the presence of polyethylene glycol \cite{26,27,28,29,30,31}. Whilst the continuous description of the overdamped active biofilaments can be postulated on symmetry grounds, \cite{32,33} it can also be derived by rigorously coarse-graining a specific underlying microscopic model \cite{34,35}. This avenue – which has also been often used for systems of self-propelled particles \cite{36} – is useful as it allows one to determine the effective parameters of the continuum theory in terms of the geometrical and physical quantities appearing in the microscopic model. Here, we follow this approach and consider a caricature model of a MT-MM mixture, inspired by actin-myosin \cite{37,38} and MT-kinesin/dynein \cite{39,40,41,42,43} systems. While missing many specific biological ingredients, our model instead focuses on the symmetries of the microscopic interactions that, ultimately, define the universality class of Eqs. (1) and (2). Since most of the experiments either studied MT-MM mixtures directly on surfaces \cite{44,45,46,47} or observed spontaneous clustering of bulk systems onto interfaces \cite{48}, we consider our model in 2D.

We treat MTs as rigid rods of fixed length \( l \) with distinct ends, denoted as “+” and “−”, and consider “+”-directed MMs, which are described by their distribution along individual MTs, as detailed below. Unlike in MT motility assays \cite{49} (where MTs are self-propelled), in MT-MM mixtures microtubular rods possess no constant velocity. Instead, filaments can only change position and orientation due to either thermal diffusion, or motor-mediated interactions.

The nature of motor-mediated interactions between filaments depends on the underlying microscopic detail. For instance, it was demonstrated that MMs able to associate with two filaments simultaneously can either cluster MTs, or actively separate them, depending on the initial configuration (Fig. 1). Importantly, our dynamics captures both possible outcomes – consistent with the current view of most kinesin motors \cite{31,44}, and unlike previous work \cite{47} which solely focused on the case of polar clustering. Specifically, our interaction rule is the following. If the initial relative angle between rods exceeds some critical value (in our case \( \pi/2 \)) then MTs first align in an anti-parallel way and then slide apart. Otherwise, MTs cluster to acquire the same position and orientation (Fig. 1b).

Within our model, MTs are covered by a steady-state static distribution of motors. Motor coverage may either be homogeneous or inhomogeneous \cite{50,51}, and is parametrized by two geometrical quantities: \( \Xi = \frac{(m^+ - m^-)}{(2m^-)} \), and \( \tau_0 \) \( (m^+ \text{ and } m^- \text{ denote motor concentrations at the two ends of a MT, Fig. 1b). Hereafter, we refer to } \Xi = 0 \text{ and } \Xi \neq 0 \text{ as the isotropic and anisotropic cases, respectively.} \)

In what follows, we work in two-dimensional Cartesian coordinates. Assuming that motor-induced rearrangements of MTs are fast with respect to diffusion, we treat them as instantaneous collisions. The probability distribution function, \( P(r, \phi) \), for a MT to be at a position \( r \) with an orientation \( \mathbf{n} = (\cos \phi, \sin \phi) \), given by the angle \( \phi \), obeys the following Boltzmann-like kinetic equation

\[
\dot{c} P(r, \phi) = D_r \partial_r^2 P(r, \phi) + \partial_r D_r \partial_r P(r, \phi) \\
+ \int d\xi \left[ \frac{\delta}{\delta \xi} \int_{-\frac{\pi}{2}}^{\frac{\pi}{2}} d\omega W_i^+ P(r_1, \phi_1) P(r_2, \phi_2) \right] \\
+ \int d\omega W_i^- P(r_1, \phi_1) P(r_2, \phi_2) \\
- \int d\xi \int_{-\frac{\pi}{2}}^{\frac{\pi}{2}} d\omega W^0 P(r, \phi) P(r - \xi, \phi - \omega). \tag{3}
\]

The first two terms on the r.h.s. of Eq. (3) represent contributions from diffusion, where \( D_r \) is the rotational diffusion coefficient and \( D_{ij} \) are components of the translational diffusion tensor \cite{52,53}. The rest of the equation encodes our collision rules between MTs, and includes clustering and sliding, see Figure 1. The positions of the colliding MTs are given by \( r_{i,j} = r + \frac{\pi}{2} \), while their orientations are defined by the angles \( \phi_{1,2} = \phi \pm \frac{\pi}{2} \), \( \xi \) and \( \omega \) parametrise separations between MT centres and their orientations, respectively. The parameter \( \eta \) determines the final relative displacement of MTs after sliding – henceforth we consider \( \eta = 1 \), corresponding to full separation. For needle-like MTs considered here, the collision rates \( W_i^+, W_i^- \) \( W^- \) only differ from zero when two MTs intersect in 2D; see \cite{54,55} for their explicit dependence on \( \xi, \omega, \Xi \), and \( \tau_0 \). Also, we note here that while the value \( \pi/2 \) of the critical angle separating clustering and sliding dynamics of MTs is hard-wired into our theory, some idea of phase behaviour corresponding to different values of that angle can be obtained by using \( \eta \neq 1 \). We performed exploratory simulations with \( \eta \) in the range between 1 and 0.5 and found no qualitative difference with the phase behaviour reported below.

We proceed by applying a rigorous coarse-graining procedure developed in \cite{56} to Eq. (3) to derive a system of mean-field equations for the density of filaments \( \rho \), their mean orientation \( p_\phi \), and the nematic tensorial field \( Q_{ij} \). These variables are defined as the
first three moments of $P(r, \phi)$:

$$
\rho(r) = \frac{1}{2\pi} \int_0^{2\pi} P(r, \phi) d\phi, \quad p_i(r) = \frac{1}{2\pi} \int_0^{2\pi} n_i P(r, \phi) d\phi, \quad Q_{ij}(r) = \frac{1}{2\pi} \int_0^{2\pi} n_i n_j - \frac{1}{2} \delta_{ij} P(r, \phi) d\phi.
$$

where $i, j = \{x, y\}$, and we introduced dimensionless units. The resulting equations contain a very large number of terms, as is often the case with kinetic theories, and their explicit form is given in (1). To study the dynamics predicted by this approach, we perform numerical simulations of the hydrodynamic equations and discuss representative results below (see Fig. 2). Simulations are initialised from an isotropic uniform MT suspension with overall density $\rho_0$ and a small amount of noise. Without loss of generality, we set $\tau_0 = 1/2$, and vary $\Xi$ and $\rho_0$.

A linear stability analysis shows that the uniform isotropic state is linearly unstable towards the emergence of a globally-ordered nematic state, when $\rho_0 > \rho_{cr} = 6\pi/(1 + \Xi(1 - \rho_0))$. Additionally, for $\rho_{cr} < \rho_0 < \rho_\infty$, this nematic state is itself unstable. Simulations demonstrate that the latter instability leads to co-existence between high-density, nematically-ordered elongated domains and a low-density isotropic background (Fig. 2a and Suppl. Movie 1). The outcome of this phase separation at late times depends on the value of the anisotropy parameter, $\Xi$. For small $\Xi$, domains coarsen to leave a single static band, whose size scales with the system size (Fig. 2b). Inside the band, MTs are ordered nematically, with residual polar order confined at the interface with the isotropic phase. For large enough $\Xi$, we instead observe an ever-evolving pattern (Fig. 2c and Suppl. Movie 2), superficially reminiscent of “active turbulence” in wet active gels. To characterise the properties of this spatiotemporal pattern, which we call dry active turbulence, we plot the time evolution of the domain size, computed via the first moment of the structure factor and its Fourier transform (Figs. 2 and 3 respectively). It is apparent that there is a selected lengthscale in the isotropic case, while the dynamics in the anisotropic case appear to be chaotic (as the Fourier transform in Fig. 2 contains all frequencies). Our findings are summarised in the phase diagram in Figure 2.

The kinetic pathway associated with dry active turbulence becomes apparent in simulations with smaller domains (Fig. 2d, Suppl. Movie 3). These shows that the self-assembled nematically ordered MT bands undergo a cyclic process where they stretch perpendicular to their long direction, rotate, stretch and split, to reform later on. This process is quasi-periodic in smaller system, but appears to be chaotic in larger ones.

To identify the fundamental mechanism leading to pattern formation in our system, we now search for a minimal model. We define the latter as a set of simple equations, which simultaneously satisfies two conditions. First, it needs to have qualitatively similar dynamics as the full model (Figs. 2a and b); it should retain both a transition between a uniform and a phase separated nematic state, as well as a regime with chaotic dynamics; in small domains, it should exhibit features similar to Figure 2. Second, we require that the location of the phase boundaries in the minimal and full models (Figs. 2d and e), is quantitatively similar. As a first step, we explore the observation that polar order plays a minor role (Fig. 2c), and adiabatically eliminate $p_i$ in favour of $\partial_\rho \rho$ and $\partial_\rho Q_{ij}$, keeping only the lowest order terms in spatial gradients (as in a hydrodynamic expansion). Then, we systematically switch off each term individually in the resulting equations, and compute the phase diagram; the term is only reinstated if its exclusion leads to a substantial change in the phase boundary location.

This procedure yields the minimal model defined in Eqs. (1) and (2), and its phase diagram is presented in Figure 2. The eight constants $\mu$, $\chi$, $\lambda$, $\alpha$, $\xi$, $\beta_1$, $\beta_2$ – are not arbitrary, and are explicitly derived in terms of the microscopic parameters $\rho_0$, $\Xi$, $\tau_0$ and $\eta$ (see SI for details). Within this set, $\xi$ is the only parameter that can change sign – the others are always positive.

We now discuss the physical meaning of each term in Eqs. (1) and (2). First, $\mu$ and $\lambda$ determine the non-equilibrium chemical potential of our mixture: their main role is to set the values of the densities in the isotropic and nematic phases. Next, $\alpha$ is a non-equilibrium Landau coefficient setting the magnitude of order in the bulk (together with the term 4($\rho/p_{cr} - 1$) $Q_{ij}$), while $\kappa$ is the nematic elastic constant. Similar terms are also present in a purely passive Model describing, for instance, phase separation in passive liquid crystals. The key qualitative ingredients that produce chaotic behaviour in our model are the terms proportional to $\chi$ and $\xi$, $\beta_1$ and $\beta_2$. Among them, $\chi$ is an “extensile flux”, whose role is similar to that of an extensile stress in active gels. This term enhances diffusion along the direction of the local nematic order (i.e., the eigenvector of $Q_{ij}$ corresponding to its positive eigenvalue), and decreases it along the perpendicular direction. Second, $\xi$ creates an effective torque at the interface, as the associated term depends on density gradients, which are largest at the interface. When $\xi$ is positive (negative), it tends to orient MTs parallel (perpendicular) to an isotropic-nematic interface. Finally, $\beta_1$ and $\beta_2$ create modulation of the nematic ordering (i.e., the positive eigenvalue of $Q_{ij}$). These terms promote activity-induced disorder, and act similarly to a negative elastic constant. Additionally, they contribute to the interfacial torque at the boundary of a nematic band, where $Q_{ij}Q_{kl}$ drops sharply to zero, following the density field. While similar terms could in principle be derived from an effective free energy, a thermodynamic framework would lead to additional constraints between the values of $\beta_1$ and $\beta_2$.

The minimal model is now simple enough for us to dissect the mechanisms underlying pattern formation. The kinetic pathway leading to non-equilibrium phase separation proceeds as follows. Starting from a uniform disordered solution with $\rho > p_{cr}$, MTs rapidly acquire orientational order, through the Landau coupling in Eq. (2). At this point, the extensile active flux, arising from MT sliding, enhances diffusion along the nematic direction, and hinders it perpendicularly. When this effect is strong enough, the perpendicular diffusion becomes effectively negative, causing MTs to 

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$^\dagger$ Here we generically use the term “model C” to describe a set of equations coupling the dynamics of a conserved field to that of a non-conserved one.
Second, when $\Xi$ is sufficiently large, the $\beta_{1,2}$ terms dominate over both the restoring elastic constant $\kappa$ and the $\zeta$ term: the associated torque rotates the MTs at the nematic-isotropic interface, so that they tend to orient perpendicular to the band border. This interfacial alignment conflicts with the direction of the nematic order within the bulk of the band; it couples to the extensile flux to yield locally synchronous rotation (and stretching) of nematic bands as observed in our simulations. This cycle repeats, creating a never-settling pattern, as seen in our simulations in the dry active turbulent regime (Figs. 2 and 4a, and Suppl. Movies 3 and 5). As the sense of the emerging band rotation (clockwise or anticlockwise) is selected by spontaneous symmetry breaking, it may be different in different regions of our simulation domain, yielding a chaotic pattern (Fig. 3b, Suppl. Movies 2 and 6). Measuring the time evolution of the domain size in this regime yields statistically the same results as for the full model (Figs. 2g and h).

There is also a second mechanism that can destabilise a homogeneous nematic state, again dependent on $\beta_{1,2}$. A linear stability analysis starting from the uniform nematic phase\cite{15} shows that when these terms are large enough, they trigger the development of a modulation in $Q_{ij}$ — in the direction parallel to that of the nematic order, for $\beta_{1,2} > 0$. This instability is independent of density fluctuations and ultimately fragments the nematic phase into infinitely small microdomains. This pathway to chaos is related to that identified in\cite{19} for dry active matter with near-uniform density. However, in our model this instability is only relevant for $\rho_0 \gg \rho_{cr}$, and for lower $\rho_0$ is superseded by the turbulent phase separation dynamics discussed above.

While our minimal model is the result of a systematic coarse-graining, we can view Eqs. (1) and (2), more generally, as a phenomenological model that contains the lowest terms of the correct tensorial nature\cite{54}. Upon coarse-graining, a microscopic model within the same universality class as the one studied here would, therefore, provide the expressions for the parameters in Eqs. (1) and (2), but would not generate extra terms. Indeed, setting $\beta_{1,2} = \lambda = \mu = 0$ shows that our equations, in this limit, reduce to the minimal model for flocking of self-propelled particles with nematic order\cite{8,14,15,48}. We, therefore, propose Eqs. (1) and (2) as a unifying model for dry active systems with nematic order. Recently, similar arguments were used to propose active versions of Models B and H\cite{13} in Hohenberg-Halperin classification\cite{51}. We follow this analogy and refer to Eqs. (1) and (2) as active Model C. This model is in a different universality class with respect to active gel theory\cite{11}, which exhibits instabilities in an active nematic fluid with constant density, whereas in our case patterns are always associated with a non-equilibrium phase separation. We want to stress that while previous work reported types of chaotic behaviour similar to the limiting cases of our model, either based on hydrodynamic\cite{8} or kinetic theories\cite{9,13,51}, active model C unifies all this into a general universality class.

Analysis of active Model C with phenomenological coefficients re-enforces our physical interpretation of the instability modes. First, nematic-isotropic phase separation also occurs with $\zeta = \beta_{1,2} = 0$, confirming that this phenomenon relies solely on a non-zero extensile flux, $\chi \neq 0$ (Fig. 3c, Suppl. Movie 7). Second, setting $\chi = 0$ whilst retaining $\beta_{1,2}$ and $\zeta$ only leads to a uniform nematic phase, confirming that $\chi$ is necessary for any patterning (Suppl. Movie 8). Third, switching off only $\zeta$ leads to chaotic...
Fig. 3 Pattern formation within the minimal model. (a) Chaotic dynamics similar to Figure 2b (ζ = 0.1, τ0 = 0.5). (b) Chaotic dynamics for larger system size and anisotropy (ζ = 0.3, τ0 = 0.5). (c) Non-equilibrium phase separation with β1,2 = ζ = 0 (ζ = 0). (d) Chaotic dynamics with ζ = 0 (ζ = 0). (e) Interfacial undulation and chaos with β1,2 = 0 (ζ = 0). For all plots p0 = 1.1β1, scale bar: 10 μm.

For various values of its parameters, active Model C serves as a catalogue of patterns in dry active systems. As mentioned above, a sub-set of terms in Eqs. (1) and (2) was obtained in models of flocking of self-propelled particles with nematic order.\textsuperscript{[14,15]} Within those models, rigorous coarse-graining shows that χ and ζ are both positive and, accordingly, the generic outcome found by numerical simulations\textsuperscript{[12,13]} is non-equilibrium phase separation and chaos through band undulations (as in Fig. 3e). Based on our phenomenological model and interpretation, we also expect dry active turbulence with contractile active flux, χ < 0, and interfacial torques favouring parallel alignment at the interface, as would occur when ζ, or β1,2 are positive. This scenario may be relevant for pattern formation in MT-MM mixtures where the underlying microscopic collision rules differ from those in Figure 1. Further work is required to identify the criteria for a microscopic model to belong to the universality class of our active Model C.

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Conflicts of interest
There are no conflicts to declare.

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