Abstract

The IBM translation models have been hugely influential in statistical machine translation; they are the basis of the alignment models used in modern translation systems. Excluding IBM Model 1, the IBM translation models, and practically all variants proposed in the literature, have relied on the optimization of likelihood functions or similar functions that are non-convex, and hence have multiple local optima. In this paper we introduce a convex relaxation of IBM Model 2, and describe an optimization algorithm for the relaxation based on a subgradient method combined with exponentiated-gradient updates. Our approach gives the same level of alignment accuracy as IBM Model 2.

1 Introduction

The IBM translation models (Brown et al., 1993) have been tremendously important in statistical machine translation (SMT). The IBM models were the first generation of SMT systems; in recent work, they play a central role in deriving alignments used within many modern SMT approaches, for example phrase-based translation models (Koehn, 2008) and syntax-based translation systems (e.g., (Chiang, 2005; Marcu et al., 2006)). Since the original IBM paper, there has been a large amount of research exploring the original IBM models and modern variants (e.g., (Moore, 2004; Liang et al., 2006; Toutanova and Galley, 2011; Riley and Gildea, 2012; Vogel et al., 1996)).

Excluding IBM Model 1, the IBM translation models, and practically all variants proposed in the literature, have relied on the optimization of likelihood functions or similar functions that are non-convex. Unfortunately, non-convex objective functions have multiple local optima, and finding a global optimum of a non-convex function is typically a computationally intractible problem. Typically, an EM algorithm is used, which often runs in a reasonable amount of time, but with no guarantees of finding a global optima (or for that matter, even a near-optimal solution).

In this paper we make the following contributions:

• We introduce a convex relaxation of IBM Model 2. At a very high level, the relaxation is derived by replacing the product $t(f_j|e_i) \times d(i|j)$ with a relaxation that is commonly used in the linear programming literature (e.g., see (Bertsimas, 1997; Bertsimas and Tsitsiklis, 1997; Martins et al., 2010)). (Here $t(f|e)$ are the translation parameters of the model, and $d(i|j)$ are the distortion parameters; the product is non-linear, effectively introducing non-convexity into the problem.)

• We describe an optimization algorithm for the relaxed objective, based on a combination of stochastic subgradient methods with the exponentiated-gradient (EG) algorithm (Kivinen and Warmuth, 1997; Beck and Teboulle, 2003).

• We describe experiments with the method on standard alignment datasets, showing that the EG algorithm converges in only a few passes over the data, and that our method achieves accuracies that are very similar to those of IBM Model 2.

Framing the unsupervised learning of alignment models as a convex optimization problem, with guaranteed convergence to a global optimum, has several clear advantages. First, the method is easier to analyze, as the objective function is being truly maximized. Second, there is no need for initialization heuristics with the approach, given that the method will always converge to a global optimum. Finally, we expect that our convexity-based approach may facilitate the further development of more convex models. There has been a rich
interplay between convex and non-convex methods in machine learning: as one example consider the literature on classification problems, with early work on the perceptron (linear/convex), then work on neural networks with back-propagation (non-linear/non-convex), then the introduction of support vector machines (non-linear/convex), and finally recent work on deep belief networks (non-linear/non-convex). In view of these developments, the lack of convex methods in translation alignment models has been noticeable, and we hope that our work will open up new directions and lead to further progress in this area.

Notation. Throughout this paper, for any integer $N$, we use $[N]$ to denote $\{1 \ldots N\}$ and $[N]_0$ to denote $\{0 \ldots N\}$.

2 Related Work

(Brown et al., 1993) introduced IBM Models 1 through 5, and optimization methods for these models based on the EM algorithm. While the models were originally introduced for full translation, they are now mainly used to derive alignments which are then used by phrase-based and other modern SMT systems. Since the original IBM models were introduced, many variants have been introduced in the literature. (Vogel et al., 1996) introduced a model, sometimes referred to as IBM 2.5, which uses a parameterization that is similar to a hidden Markov model, and which allows the value of each alignment variable to be conditioned on a previous alignment variable. (Liang et al., 2006) describe a method that explicitly incorporates agreement preferences during training. (Och and Ney, 2003) give a systematic comparison of several alignment models in the literature. (Moore, 2004) gives a detailed study of IBM Model 1, showing various steps that can be used to improve its performance. (Ganchev et al., 2010) describes a method based on posterior regularization that incorporates additional constraints within the EM algorithm for estimation of IBM models. All of these approaches are unsupervised, in that they do not require labeled alignment data; however several authors have considered supervised models (e.g., see (Lacoste-Julien et al., 2006; Taskar et al., 2005; Haghigihi et al., 2009)). The focus of the current paper is on unsupervised learning; the unsupervised variants described above all make use of non-convex objective functions during training, with the usual problems with multiple local maxima.

3 The IBM Model 1 and Model 2

Optimization Problems

In this section we give a brief review of IBM Models 1 and 2, and the optimization problems arising from these models. The standard approach for optimization within these models is the EM algorithm.

Throughout this section, and the remainder of the paper, we assume that our set of training examples is $(e^{(k)}, f^{(k)})$ for $k = 1 \ldots n$, where $e^{(k)}$ is the $k$'th English sentence and $f^{(k)}$ is the $k$'th French sentence. Following standard convention, we assume the task is to translate from French (the “source” language) into English (the “target” language). We use $E$ to denote the English vocabulary (set of possible English words), and $F$ to denote the French vocabulary. The $k$'th English sentence is a sequence of words $e_1^{(k)} \ldots e_{l_k}^{(k)}$ where $l_k$ is the length of the $k$'th English sentence, and each $e_i^{(k)} \in E$; similarly the $k$'th French sentence is a sequence $f_1^{(k)} \ldots f_{m_k}^{(k)}$ where each $f_i^{(k)} \in F$. We define $e_0^{(k)}$ for $k = 1 \ldots n$ to be a special NULL word (note that $E$ contains the NULL word). Finally, we define $L = \max_{k=1}^n l_k$ and $M = \max_{k=1}^n m_k$.

For each English word $e \in E$, we will assume that $D(e)$ is a dictionary specifying the set of possible French words that can be translations of $e$. The set $D(e)$ is a subset of $F$. In practice, $D(e)$ can be derived in various ways; in our experiments we simply define $D(e)$ to include all French words $f$ such that $e$ and $f$ are seen in a translation pair.

Given these definitions, the IBM model 2 optimization problem is given in Figure 1. The parameters in this problem are $t(f|e)$ and $d(i|j)$. The $t(f|e)$ parameters are translation parameters specifying the probability of English word $e$ being translated as French word $f$. The distortion parameters $d(i|j)$ specify the probability of the $j$'th French word in a sentence being aligned to the $i$'th English word. We use a variant of IBM Model 2 where the distortion variables are shared across all sentence lengths (similar variants have been used in (Liang et al., 2006) and (Koehn, 2008)). The objective function is then
The objective function for IBM Model 1 is actually convex, the distortion parameters \( d(i|j) \) are all fixed to be the uniform distribution (i.e., \( 1/(L+1) \)). The objective function for IBM Model 1 is actually convex, so the EM algorithm will converge to a global maximum. However IBM Model 1 is much weaker than model 2, and typically gives far worse performance. In our experiments, and which performs well in experiments. A common heuristic is to initialize the \( t(f|e) \) parameters in EM optimization of IBM Model 2 using the output from IBM Model 1. The intuition behind this heuristic is that the IBM Model 1 values for \( t(f|e) \) will be a reasonable starting point, and the EM algorithm will climb to a “good” local optimum. We are not aware of any guarantees for this initialization heuristic, however.

### 4 A Convex Relaxation of IBM Model 2

We now introduce a convex optimization problem, the I2CR (IBM 2 Convex Relaxation) problem. As its name suggests, this optimization problem is closely related to IBM Model 2, but is convex. Because of this it will be relatively easy to derive an optimization algorithm that is guaranteed to converge to a global optimum. Our experiments show that the relaxation gives very similar performance to the original IBM 2 optimization problem, as described in the previous section.

We first describe an optimization problem, I2CR-1, that illustrates the basic idea behind the convex relaxation. We then describe a refined relaxation, I2CR-2, that introduces a couple of modifications, and which performs well in experiments.
Input: Define $E$, $F$, $L$, $M$, $(e^{(k)}, f^{(k)}, l_k, m_k)$ for $k = 1 \ldots n$, $D(e)$ for $e \in E$ as in Section 3.

Parameters:

- A parameter $t(f|e)$ for each $e \in E, f \in D(e)$.
- A parameter $d(i|j)$ for each $i \in [L], j \in [M]$.
- A parameter $q(i, j, k)$ for each $k \in [n], i \in [l_k], j \in [m_k]$.

Constraints:

$$\forall e \in E, f \in D(e), \quad t(f|e) \geq 0 \quad (9)$$
$$\forall e \in E, \quad \sum_{f \in D(e)} t(f|e) = 1 \quad (10)$$
$$\forall i \in [L], j \in [M], \quad d(i|j) \geq 0 \quad (11)$$
$$\forall j \in [M], \quad \sum_{i \in [L]} d(i|j) = 1 \quad (12)$$

$$\forall i, j, k, \quad q(i, j, k) \geq 0 \quad (13)$$
$$\forall i, j, k, \quad q(i, j, k) \leq d(i|j) \quad (14)$$
$$\forall i, j, k, \quad q(i, j, k) \leq t(f^{(k)}|e^{(k)}_i) \quad (15)$$

Objective: Maximize

$$\frac{1}{n} \sum_{k=1}^{n} \sum_{j=1}^{m_k} \log \sum_{i=0}^{l_k} q(i, j, k) \quad (16)$$

with respect to the $q(i, j, k), t(f|e)$ and $d(i|j)$ parameters.

Figure 3: The I2CR-1 (IBM 2 Convex Relaxation) Problem, version 1.

4.1 The I2CR-1 Problem

The I2CR-1 problem is shown in Figure 3. A first key idea is to introduce a new variable $q(i, j, k)$ for each $k \in [n], i \in [l_k], j \in [m_k]$: that is, a new variable for each triple $(i, j, k)$ specifying a sentence pair, and a specific English and French position in that sentence. Each $q$ variable must satisfy the constraints in Eqs. 13-15, repeated here for convenience:

$$\forall i, j, k, \quad q(i, j, k) \geq 0 ,$$
$$\forall i, j, k, \quad q(i, j, k) \leq d(i|j) ,$$
$$\forall i, j, k, \quad q(i, j, k) \leq t(f^{(k)}|e^{(k)}_i) .$$

The objective function is

$$\frac{1}{n} \sum_{k=1}^{n} \sum_{j=1}^{m_k} \log \sum_{i=0}^{l_k} q(i, j, k)$$

which is similar to the objective function in Figure 1, but where $t(f^{(k)}|e^{(k)}_i) \times d(i|j)$ has been replaced by $q(i, j, k)$. The intuition behind the new problem is as follows. If, instead of the constraints in Eqs. 13-15, we had the constraint

$$q(i, j, k) = t(f^{(k)}|e^{(k)}_i) \times d(i|j) , \quad (17)$$

then the I2CR-1 problem would clearly be identical to the IBM Model 2 optimization problem. We have used a standard relaxation of the non-linear constraint $x = y \times z$ where $x, y, z$ are all variables in the range $[0, 1]$, namely

$$x \leq y ,$$
$$x \leq z ,$$
$$x \geq y + z - 1 .$$

These inequalities are a relaxation in the sense that any $(x, y, z)$ triple that satisfies $x = y \times z$ also satisfies these constraints. Applying this relaxation to Eq. 17 gives

$$q(i, j, k) \leq t(f^{(k)}|e^{(k)}_i) ,$$
$$q(i, j, k) \leq d(i|j) ,$$
$$q(i, j, k) \geq t(f^{(k)}|e^{(k)}_i) + d(i|j) - 1 . \quad (18)$$

The final thing to note is that the constraint in Eq. 18 can be omitted in the I2CR-1 problem. This is because the task is to maximize the objective with respect to the $q$ variables and the objective is strictly increasing as the $q$ values increase—thus lower bounds on their values are redundant in the I2CR-1 problem.

It is easily verified that the constraints in the I2CR-1 problem are linear, and that the objective function is convex. In Section 5 of this paper we describe an optimization method for the problem.

Note that because the objective function is being maximized, and the objective increases monotonically as the $q$ values increase, at the global optimum\(^1\)
Input: Same as in I2CR-1 (Figure 4).
Parameters: Same as in I2CR-1 (Figure 4).

Constraints: Same as in I2CR-1 (Figure 4).
Objective: Maximize

\[
\frac{1}{2n} \sum_{k=1}^{n} \sum_{j=1}^{m_k} \log' \sum_{i=0}^{l_k} q(i, j, k) \\
+ \frac{1}{2n} \sum_{k=1}^{n} \sum_{j=1}^{m_k} \log' \sum_{i=0}^{l_k} t(f_j(k)|e_i(k)) \\
(\log(x) + \log(y) = \log(xy))
\]

with respect to the \( q(i, j, k), t(f|e) \) and \( d(i|j) \) parameters.

Figure 4: The I2CR-2 (IBM 2 Convex Relaxation) Problem, version 2. The problem is identical to the I2CR-1 problem, but it also includes a term in the objective function that is identical to the IBM Model 2 objective. We define \( \log'(z) = \log(z + \lambda) \) where \( \lambda \) is a small positive constant.

we have

\[
q(i, j, k) = \min \{ t(f_j(k)|e_i(k)), d(i|j) \},
\]

where \( \min \{ x, y \} \) returns the minimum of the two values \( x \) and \( y \). Thus, we could actually eliminate the \( q \) variables and write an optimization problem that is identical to the IBM Model 2 optimization problem, but with the objective function

\[
\frac{1}{n} \sum_{k=1}^{n} \sum_{j=1}^{m_k} \log \sum_{i=0}^{l_k} \min \{ t(f_j(k)|e_i(k)), d(i|j) \}.
\]

It will turn out that both views of the I2CR-1 problem—with and without the \( q \) variables—are helpful, so we have included both in this paper.

4.2 The I2CR-2 Problem

Figure 4 shows the refined optimization problem, which we call I2CR-2. The problem incorporates two modifications. First, we modify the objective function to be

\[
\frac{1}{2n} \sum_{k=1}^{n} \sum_{j=1}^{m_k} \log' \sum_{i=0}^{l_k} q(i, j, k) \\
+ \frac{1}{2n} \sum_{k=1}^{n} \sum_{j=1}^{m_k} \log' \sum_{i=0}^{l_k} t(f_j(k)|e_i(k)) \\
(\log(x) + \log(y) = \log(xy))
\]

Thus the objective function includes a second term that is identical to the objective function for IBM Model 1 (see Figure 2). In preliminary experiments with the I2CR-1 optimization problem, we found that the I2CR-1 objective was not sufficiently dependent on the \( t \) parameters: intuitively, if the \( d \) parameters achieve the \( \min \) on many training examples, the values for the \( t \) variables become unimportant. The addition of the IBM Model 1 objective fixed this problem by introducing a term that depends on the \( t \) values alone.

Second, we replace \( \log \) by \( \log' \), where \( \log'(z) = \log(z + \lambda) \), and \( \lambda \) is a small positive constant (in our experiments we used \( \lambda = 0.001 \)). Under this definition the derivatives of \( \log' \) are upper-bounded by \( 1/\lambda \), in contrast to \( \log \), where the derivatives can diverge to infinity. The optimization methods we use are gradient-based methods (or more precisely, subgradient-based methods), and we have found them to be considerably more stable when the values for gradients do not diverge to infinity.

The modified objective remains convex.

5 A Stochastic Exponentiated-Gradient Algorithm for Optimization

We now describe an algorithm for optimizing the I2CR-2 problem in Figure 4. The algorithm is closely related to stochastic gradient ascent, but with two modifications:

- First, because the \( t(f|e) \) and \( d(i|j) \) parameters have simplex constraints (see Figure 1), we use exponentiated gradient (EG) updates. EG algorithms are gradient-based methods that maintain simplex constraints; see for example: (Kivinen and Warmuth, 1997; Beck and Teboulle, 2003; Collins et al., 2008).

- Second, the objective function in the I2CR-2 problem is convex, but is not differentiable (the gradient may not exist at all points). For this reason we use subgradients in the place of gradients. In spite of the non-differentiability of the objective function, subgradient methods still have strong convergence guarantees when combined with EG updates (e.g., the convergence proofs in (Beck and Teboulle, 2003)
To derive the updates, recall that we are maximizing the following objective function:

\[
h(t, d) = \frac{1}{2|\mathcal{T}|} \sum_{k \in \mathcal{T}} \sum_{j=1}^{m_k} \log \sum_{i=0}^{l_k} \min \left\{ t(f_j^{(k)}|e_i^{(k)}), d(i|j) \right\}
\]

and

\[
\nabla d(i|j) = \frac{1}{2|\mathcal{T}|} \sum_{k: i,j \leq l_k, j \leq m_k} \frac{1 - I(i, j, k)}{Q(j, k)} .
\]

Exponentiated-gradient updates then take the following form:

\[
t(f|e) \leftarrow \frac{t(f|e) \times \exp \{ \gamma \times \nabla t(f|e) \}}{\sum_{j} t(f|e) \times \exp \{ \gamma \times \nabla t(f|e) \}}
\]

and

\[
d(i|j) \leftarrow \frac{d(i|j) \times \exp \{ \gamma \times \nabla d(i|j) \}}{\sum_{i} d(i|j) \times \exp \{ \gamma \times \nabla d(i|j) \}}
\]

where \( \gamma > 0 \) is a constant step size in the algorithm. Note that the EG updates make use of subgradients, but maintain the simplex constraints on the \( t \) and \( d \) variables.

The method just described is a batch gradient method, where the entire training set \( \mathcal{T} = \{1 \ldots n\} \) is used to derive the subgradients before the updates in Eqs. 20 and 21 are made. Many results in machine learning and NLP have shown that stochastic gradient methods, where a subset of the training examples is used before each gradient-based update, can converge much more quickly than batch gradient methods. In our notation, this simply involves replacing \( \mathcal{T} \) by some subset \( \mathcal{T}' \) of the training examples in the above definitions, where \( |\mathcal{T}'| \) is typically much smaller than \( |\mathcal{T}| \).

Figure 5 shows our final algorithm, a stochastic version of the exponentiated-gradient method. The method takes \( S \) passes over the data. For each pass, it randomly partitions the training set into mini-batches \( \mathcal{T}_1 \ldots \mathcal{T}_K \) of size \( B \), where \( B \) is an integer specifying the size of each mini-batch (in our experiments we used \( B = 125 \) or \( B = 250 \)). The algorithm then performs EG updates using each mini-batch \( \mathcal{T}_1 \ldots \mathcal{T}_K \) in turn. As can be seen in Table 3, our experiments show that the algorithm makes very significant progress in the first pass over the data, and takes very few iterations to converge to a good solution even though we initialized with uniform parameter values.

6 Experiments

In this section we describe experiments using the I2CR-2 optimization problem combined with the
1: **Input:** Define $E$, $F$, $L$, $M$, $(e^{(k)}, f^{(k)}, t_k, m_k)$ for $k = 1 \ldots n$, $D(e)$ for $e \in E$ as in Section 3.

An integer $B$ specifying the batch size. An integer $S$ specifying the number of passes over the data. A step size $\gamma > 0$. A parameter $\lambda > 0$ used in the definition of $\log^\gamma$.

2: **Parameters:**
   - A parameter $t(f|e)$ for each $e \in E$, $f \in D(e)$.
   - A parameter $d(i|j)$ for each $i \in [L]_0$, $j \in [M]$.

3: **Definitions:**

   $$R(j, k) = \lambda + \sum_{i=0}^{l_k} t(f_j^{(k)}|e_i^{(k)})$$

   $$Q(j, k) = \lambda + \sum_{i=0}^{l_k} \min\{t(f_j^{(k)}|e_i^{(k)}), d(i|j)\}$$

4: **Initialization:**
   - $\forall e \in E$, $f \in D(e)$, $t(f|e) = 1/|D(e)|$
   - $\forall j \in [M]$, $i \in [L]_0$, $d(i|j) = 1/(L + 1)$

5: **Algorithm:**
   - for all $s = 1$ to $S$
     - Randomly partition $[n]$ into subsets $\mathcal{T}_1 \ldots \mathcal{T}_K$ of size $B$ where $K = n/B$.
   - for all $b = 1$ to $K$
     - for all $j = 0$ to $l_k$
       - $\alpha(e_i^{(k)}, f_j^{(k)}) := 1/(2R(j, k))$

   if $t(f_j^{(k)}|e_i^{(k)}) \leq d(i|j)$ then
     - $\alpha(e_i^{(k)}, f_j^{(k)}) := 1/(2Q(j, k))$
   else
     - $\beta(i, j) := 1/(2Q(j, k))$

   - for all $j = 0$ to $l_k$
     - for all $i = 0$ to $m_k$
       - $t(f_j^{(k)}|e_i^{(k)}) = t(f_j^{(k)}|e_i^{(k)}) \exp(\gamma \times \alpha(e_i^{(k)}, f_j^{(k)}) / B)$
       - $d(i|j) = d(i|j) \exp(\gamma \times \beta(i, j) / B)$

   - Renormalize $t$ and $d$ parameters to satisfy
     - $\sum_j t(f|e) = 1$ and $\sum_i d(i|j) = 1$.

6: **Output:** $t$ and $d$ parameters.

Figure 5: The stochastic exponentiated-gradient algorithm for optimization of I2CR-2.

...stochastic EG algorithm for parameter estimation. We first describe the data sets we use, and then describe experiments with the method, comparing our approach to results from IBM Model 2. We compare the various algorithms in terms of their accuracy in recovering alignments, using metrics such as F-measure and AER.

6.1 **Data Sets**

We use data from the bilingual word alignment workshop held at HLT-NAACL 2003 (Michalcea and Pederson, 2003). As a first dataset, we use the Canadian Hansards bilingual corpus, with 247,878 English-French sentence pairs as training data, 37 sentences of development data, and 447 sentences of test data (note that we use a randomly chosen subset of the original training set of 1.1 million sentences, similar to the setting used in (Moore, 2004)). The development and test data have been manually aligned at the word level, annotating alignments between source and target words in the corpus as either “sure” $(S)$ or “possible” $(P)$ alignments, as described in (Och and Ney, 2003).

As a second data set, we used the Romanian-English data from the HLT-NAACL 2003 workshop. This consisted of a training set of 48,706 Romanian-English sentence pairs, a development set of 17 sentence pairs, and a test set of 248 sentence pairs.

6.2 **Methodology**

For each of the models—IBM Model 1, IBM Model 2, and I2CR-2—we follow convention in applying the following methodology: first, we estimate the $t$ and $d$ parameters using models in both source-target and target-source directions; second, we find the most likely alignment for each development or test data sentence in each direction; third, we take the intersection of the two alignments as the final output from the model.

For the EG algorithm we use a batch size $B = 250$ and step size $\gamma = 0.5$ on the Hansards data, and $B = 125$ and $\gamma = 0.5$ for the Romanian-English data.

We report the performance of the models in terms of Precision, Recall, AER, and F-Measure as defined by (Och and Ney, 2003). If $A$ is the set of alignments produced by an algorithm, $S$ is the set of sure alignments as annotated in test data, and $P$ is the set of possible alignments, then these quantities are defined as

$$\text{Recall} = \frac{|A \cap S|}{|S|},$$
\[
\text{Precision} = \frac{|A \cap S|}{|A|}, \\
\text{AER} = 1 - \frac{|A \cap S| + |A \cap P|}{|A| + |S|}, \\
\text{F-Measure} = \frac{2 \cdot \text{Precision} \cdot \text{Recall}}{\text{Precision} + \text{Recall}}.
\]

Note that we report results in both AER and F-measure; however there is evidence (Fraser and Marcu, 2004) that F-measure is better correlated with translation quality when the alignments are used in a full system.

In training IBM Model 1 we follow (Moore, 2004) in running EM for 15 iterations. In training IBM Model 2 we first train IBM Model 1 for 15 iterations to initialize the \(t\) parameters, then train IBM Model 2 for a further 10 iterations. For the EG algorithm, we use 10 iterations over the training data for the Hansards data, and 15 iterations on the Romanian-English data (on the latter dataset results on the trial data showed that the method took slightly longer to converge). We report F-measure and AER results for each of the iterations under the IBM Model 2 and I2CR-2 models. See Table 1 for the results on the Hansards data, and Table 2 for the results on the English-Romanian dataset. It can be seen that both I2CR-2 and IBM Model 2 converge to a fairly stable result after 2-3 iterations. The two models give very similar levels of performance, for example after 10 iterations on the Hansard data IBM Model 2 gives 14.22 AER and 0.7516 F-Measure versus 14.60 AER and 0.7506 F-Measure for I2CR-2.

On the right, Table 3 shows the values of the objective function at each iteration when using the EG algorithm to optimize the I2CR-2 objective. The method makes a large amount of progress on the first iteration and then continues to improve. Finally, we note that the memory requirements for I2CR-2 and IBM2 are about the same, but that the time for one iteration of I2CR-2 on the Hansards data is approximately one hour, while the time for one iteration of IBM2 was approximately 10 minutes.

## 7 Conclusions and Future Work

We have introduced the first convex model for unsupervised learning of alignments in statistical machine translation with performance comparable to
| Iteration | EF Objective | FE Objective |
|-----------|--------------|--------------|
| 0         | -99.6053     | -79.5566     |
| 1         | -32.4528     | -27.4925     |
| 2         | -31.1641     | -26.262      |
| 3         | -30.6311     | -25.7093     |
| 4         | -30.3367     | -25.3714     |
| 5         | -30.1428     | -25.1456     |
| 6         | -30.0000     | -24.992      |
| 7         | -29.8736     | -24.8605     |
| 8         | -29.8093     | -24.7551     |
| 9         | -29.7326     | -24.684      |
| 10        | -29.6771     | -24.6099     |

Table 3: Objective values for the EG algorithm optimization of I2CR-2 at each iteration. “EF Objective” corresponds to training a model with $t(e|f)$ parameters, “FE Objective” corresponds to the reverse direction, with $t(f|e)$ parameters. Iteration 0 corresponds to the objective value under the initial, uniform parameter values.

the commonly-used IBM Model 2. We believe that introducing convexity without sacrificing performance will open the door to further improvements in this area. Future work will consider ways to speed up our algorithm and extensions of the method to more complex alignment models.

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