Constraints on Models of the Higgs Boson with Exotic Spin and Parity using Decays to Bottom-Antibottom Quarks in the Full CDF Data Set

Aaltonen, T A; Amerio, S; Amidei, D E; et al; Canelli, F; Kilminster, B; CDF Collaboration,

Abstract: A search for particles with the same mass and couplings as those of the standard model Higgs boson but different spin and parity quantum numbers is presented. We test two specific non-standard Higgs boson hypotheses: a pseudoscalar Higgs boson with spin-parity $J^P = 0^-$ and a graviton-like Higgs boson with $J^P = 2^+$, assuming for both a mass of 125 GeV/$c^2$. We search for these exotic states produced in association with a vector boson and decaying into a bottom-antibottom quark pair. The vector boson is reconstructed through its decay into an electron or muon pair, or an electron or muon and a neutrino, or it is inferred from an imbalance in total transverse momentum. We use expected kinematic differences between events containing exotic Higgs bosons and those containing standard model Higgs bosons. The data were collected by the CDF experiment at the Tevatron proton-antiproton collider, operating at a center-of-mass energy of $\sqrt{s} = 1.96$ TeV, and correspond to an integrated luminosity of 9.45 fb$^{-1}$. We observe no significant deviations from the predictions of the standard model with a Higgs boson of mass 125 GeV/$c^2$, and set bounds on the possible rate of production of each exotic state.

DOI: [https://doi.org/10.1103/PhysRevLett.114.141802](https://doi.org/10.1103/PhysRevLett.114.141802)
Constraints on models of the Higgs boson with exotic spin and parity using the full CDF data set

T. Aaltonen, S. Amerio, D. Amidei, A. Anastassov, A. Annovi, J. Antos, G. Apollinari, J.A. Appel, T. Arisawa, A. Artikov, J. Asaadi, W. Ashmanskas, B. Auerbach, A. Aurisano, F. Azfar, W. Badgett, T. Bae, A. Barbaro-Galtieri, V.E. Barnes, B.A. Barnett, P. Barria, P. Bartos, M. Bause, F. Bedeschi, S. Behari, G. Bellettini, J. Bellinger, D. Benjamin, A. Beretvas, A. Bhatti, K.R. Bland, B. Blumenfeld, A. Bocci, A. Bodek, D. Bortoletto, J. Boudreau, A. Boveia, L. Brigliadori, C. Bromberg, E. Brucken, J. Budagov, H.S. Budd, K. Burkett, G. Busetto, P. Bussey, M. Buttì, A. Buzatu, A. Calamba, S. Camarda, M. Campanelli, F. Canelli, B. Carls, D. Carlsmith, R. Carosi, A. Carrillo, B. Casal, M. Casarsa, A. Castro, P. Catastini, D. Cauz, V. Cavaliere, A. Cerri, L. Cerrito, Y.C. Chen, M. Chretk, G. Chiarelli, G. Chlachidze, K. Cho, D. Chokheli, A.Clark, C. Clarke, M.E. Convery, J. Conway, M. Corbo, M. Cordelli, C.A. Cox, D.J. Cox, M. Cremonesi, D. Cruz, J. Cuevas, R. Curletton, N. d’Ascezo, M. Datta, P. de Barbare, D. Demortier, M. Denino, M. D’Errico, F. Devoto, A. Di Canto, B. Di Ruzzaf, J.R. Dittmann, S. Donati, M. D’Onofrio, M. Dorigo, A. Driutts, K. Ebina, R. Edgar, A. Elagin, R. Erbacher, S. Errede, B. Esham, S. Farrington, J.P. Fernández Ramos, R. Field, G. Flanagan, R. Forrest, M. Franklin, J.C. Freeman, H. Frisch, Y. Funakoshi, C. Galloni, A.F. Garfinkel, P. Garosi, H. Gerberich, E. Gerchtein, S. Giagu, V. Giakoumopoulou, K. Gibson, C.M. Ginsburg, M. Giokaris, P. Giromini, V. Glagolev, D. Glenzinski, M. Gold, D. Goldin, A. Golossanov, G. Gomez, G. Gomez-Ceballos, M. Goncharov, O. González López, I. Gorelov, A.T. Goslaw, K. Gouliaos, G. Gramellini, C. Grosso-Pilcher, R.C. Group, J. Guimaraes da Costa, S.R. Hahn, J.Y. Han, F. Happpacher, K. Hara, G. Hare, R.F. Harr, T. Harrington-Taber, K. Hatakeyama, C. Hays, J. Heinrich, M. Herndon, A. Hocker, Z. Hong, W. Hopkins, S. Hou, R.E. Hughes, U. Husemann, M. Hussein, J. Huston, G. Introzzo, M. Iorio, I. Ivanov, E. James, J. Jiang, B. Jayatilaka, E.J. Jeon, S. Jindariani, M. Jones, K.K. Joo, S.Y. Jun, T.R. Jung, M. Kambeitz, T. Kamon, P.E. Karchin, A. Kasmi, Y. Kato, W. Ketchum, J. Keung, B. Kilminster, D.H. Kim, H.S. Kim, J.E. Kim, M.J. Kim, S.H. Kim, S.B. Kim, Y.J. Kim, Y.K. Kim, N. Kimura, M. Kirby, K. Knoepfel, K. Kondo, D.J. Kong, J. Konigsberg, A.V. Kotwal, M. Kreps, J. Kroll, M. Kruse, T. Kuhr, M. Kurata, A.T. Laasanen, S. Lamml, M. Lancaster, K. Lannon, G. Latino, H.S. Lee, J.S. Lee, S. Leo, S. Leone, J.D. Lewis, A. Limosani, E. Lipeles, A. Lister, H. Liu, Q. Liu, T. Liu, S. Lockwitz, A. Logino, D. Lucchesi, A. Lucà, J. Lueck, P. Lujan, P. Lukens, G. Lungen, J. Lys, R. Lysak, R. Madarak, P. Maestro, A. Malik, G. Manca, A. Manousakis-Katsikakis, L. Marchese, P. Margaroli, P. Marino, K. Matera, M.E. Mattson, M. Mazzacane, R. McNulty, A. Mehta, P. Mehtal, C. Mesropian, T. Miao, D. Mietlicki, A. Mitra, H. Miyake, S. Moed, N. Moggi, C.S. Moon, R. Moore, M. Morello, A. Mukherjee, T. Muller, P. Murat, M. Musin, J. Nachtman, Y. Naga, J. Naganama, I. Nakano, A. Napier, J. Nett, C. Neu, T. Nigman, L. Nodulman, S.Y. Noh, O. Norniella, L. Oakes, S.H. Oh, Y.D. Oh, I. Oksuzian, T. Okusawa, R. Orava, L. Ortolan, C. Pagliaire, E. Palencia, P. Palni, V. Papadimitriou, W. Parker, G. Pauletti, G. Paulini, C. Paus, T.J. Phillips, G. Piacentino, E. Pianori, J. Pilot, K. Pitts, C. Plager, L. Pondrom, S. Poprocki, K. Potamianos, A. Pranko, F. Prokoshin, F. Ptohos, G. Punzi, I. Redondo Fernández, P. Renton, M. Rescigno, F. Rimondi, L. Ristori, A. Robson, T. Rodriguez, S. Rolli, M. Ronzani, R. Roser, J.L. Rosner, F. Ruffini, A. Ruiz, J. Russ, V. Rusin, W.K. Sakamoto, Y. Sakurai, S. Santi, K. Sato, V. Saveliev, A. Savoy-Navarro, P. Schlabach, E.E. Schmidt, K. Sato, S. Schell, F. Sciri, S. Seidel, Y. Seiya, A. Semenov, F. Sforza, S.Z. Shalhout, T. Shears, P.F. Shepard, M. Shimojima, M. Shochet, I. Shirey-Aberc, A. Simonen, K. Sliwa, J.R. Smith, F.D. Snider, H. Song, V. Sorin, R. St. Denis, M. Stancari, D. Stortez, J. Strologas, Y. Sudo, A. Sukhanov, I. Suslov, K. Takemasa, Y. Takeuchi, J. Tang, M. Tecchio, P.K. Teng, J. Thom, E. Thomson, V. Thuylak, D. Toback, S. Tokar, K. Tollefsen, T. Tomura, D. Tonelli, S. Torre, D. Torretta, P. Totaro, M. Trovato, F. Ukegawa, S. Uozumi, F. Vázquez, G. Vele, C. Vellidis, C. Vernieri, M. Vidal, N.
A search for particles with the same mass and couplings as those of the standard model Higgs boson but different spin and parity quantum numbers is presented. We test two specific non-standard Higgs boson hypotheses: a pseudoscalar Higgs boson with spin-parity $J^P = 0^+$ and a graviton-like Higgs boson with $J^P = 2^+$, assuming for both a mass of 125 GeV/$c^2$. We search for these exotic states produced in association with a vector boson and decaying into a bottom-antibottom quark pair. The vector boson is reconstructed through its decay into an electron or muon pair, or an electron or muon and a neutrino, or it is inferred from an imbalance in total transverse momentum.

We use expected kinematic differences between events containing exotic Higgs bosons and those containing standard model Higgs bosons. The data were collected by the CDF experiment at the Tevatron proton-antiproton collider, operating at a center-of-mass energy of 1.96 TeV, and correspond to an integrated luminosity of 9.45 fb$^{-1}$. We observe no significant deviations from the predictions of the standard model with a Higgs boson of mass 125 GeV/$c^2$, and set bounds on the possible rate of production of each exotic state.

PACS numbers: 13.85.Rm, 14.80.Bn, 14.80.Ec

The observation of a narrow bosonic resonance $H$ with mass near 125 GeV/$c^2$ by the ATLAS [1] and CMS [2] Collaborations at the Large Hadron Collider (LHC) in the $H \rightarrow \gamma\gamma$ and $H \rightarrow ZZ \rightarrow 4\ell$ decay modes, and the evidence of such a particle at the Tevatron, primarily in association with a vector boson and in decays to bottom-antibottom quark pairs [3, 4], shifted the focus of the Higgs boson experimental program to the determination of the properties of the newly discovered particle. The central question that needs to be addressed experimentally is whether only one Higgs boson is sufficient to explain the observed data. Specifically, the spin and parity of the Higgs boson should be established in order to determine if it plays the role predicted for it by the standard model (SM) of particle physics or if it represents the first hint of more exotic interactions.

The properties of the new particle observed at the LHC are consistent with those predicted by the SM for the Higgs boson. The products of cross sections and branching ratios are as predicted [1, 5, 7]. The decays of the new particle to $ZZ^{(*)}$, $\gamma\gamma$, and $WW^{(*)}$ final states, where the asterisk indicates an off-mass-shell $Z$ or $W$ vector boson, provide excellent samples for testing its spin and parity quantum numbers $J$ and $P$, due to the measurable angular distributions of the decay products [8, 9], which depend on the quantum numbers of the decaying particle. The tests at the LHC in the bosonic decay channels exclude exotic states with spin and/or parity different from the SM prediction of $J^P = 0^+$ with high confidence level.

At the Tevatron, the primary sensitivity to the Higgs boson comes from modes in which it is produced via its coupling to vector bosons but decays to a pair of fermions. While ATLAS and CMS have reported strong evidence for fermionic decays of the Higgs boson [10, 11], spin and parity quantum numbers have not been tested in these decays. As the D0 Collaboration has shown [12], testing the spin and parity of the Higgs boson at the Tevatron provides independent information on the properties of this particle.

The Tevatron data can test alternative $J^P$ hypotheses in the $WH$, $ZH$ production modes with $H \rightarrow bb$, by examining the kinematic distributions of the observable decay products of the vector boson and the Higgs-like boson [13]. Testing the spin and parity of the Higgs boson in $H \rightarrow bb$ decays provides independent information on the properties of this particle. The models tested are described in Ref. [14]. For the SM case, Higgs boson associated production is an $S$-wave process (i.e. the $VH$ system is in a state with relative orbital angular momentum $L = 0$, where $V = W$ or $Z$), with a cross section that rises proportionally to the boson speed $\beta$ close to threshold. Here $\beta = 2p/\sqrt{s}$, where $p$ is the momentum of the Higgs boson in the $VH$ reference frame and $\sqrt{s}$ is the total energy of the $VH$ system in its rest frame [14]. In the $0^-$ case, the production is a $P$-wave process and...
the cross section rises proportionally to $\beta^3$. There are several possible $J^P = 2^+$ models, but for graviton-like models [13], the production is in a $D$-wave process, with a cross section that rises proportional to $\beta^5$. This dependence of the cross section on the spin-parity quantum numbers provides good kinematic leverage for discriminating exotic from SM Higgs boson production, since the exotic production rate is enhanced faster than the SM one at larger $\beta$, corresponding to a larger invariant mass of the final state system and higher momenta of the decay products. The models studied predict neither the ZH case, from the decay branching fraction $B(H \rightarrow b\bar{b})$. Instead, the authors suggest [13] to purify a sample of Higgs boson candidate events and to study the invariant masses of the $Wb\bar{b}$ and $Zbb$ systems, which differ strongly among the $0^+, 0^-$, and $2^+$ models.

The study of the properties of a purified signal sample with minimal sculpting of the kinematic distributions is effective at the LHC in the $H \rightarrow ZZ \rightarrow \ell^+\ell^-\ell^+\ell^-$ mode, which has a signal-to-background ratio $s/b$ exceeding 2:1. However, this is not the case for the Tevatron, where the SM Higgs boson searches typically have a $s/b$ of 1:50 [15]. With the use of multivariate analyses (MVs), small subsets of the data sample can be purified to achieve a $s/b$ ratio of $\approx 1:1$. Since the events in these subsets are selected with MVA discriminants that are functions of the kinematic properties of signal and background, their distributions are highly sculpted to resemble those predicted by the SM Higgs boson, and thus are not optimal in testing alternative models.

The strategy chosen for this Letter is to generalize the CDF searches for the SM Higgs boson in the $WH \rightarrow \ell\nu b\bar{b}$ mode [16], the $ZH \rightarrow \ell^+\ell^- b\bar{b}$ mode [17], and the $WH + ZH \rightarrow E_T b\bar{b}$ [18] mode [19], where the Z boson decays into a neutrino pair or the charged lepton from the $W$-boson decay escapes detection. In the last case, $ZH \rightarrow \ell^+\ell^- b\bar{b}$ events may be reconstructed as $E_T b\bar{b}$ events if both leptons fail to meet the identification criteria. The generalization involves searches for pseudoscalar ($J^P = 0^-$) and graviton-like ($J^P = 2^+$) bosons (denoted $X$ here), using MVA techniques similar to those developed for the SM searches. Admixtures of SM and exotic Higgs particles with indistinguishable mass are also considered, where exotic and SM production do not interfere due to different spin-parity quantum numbers. We set limits on the production rate times the decay branching ratio $B(X \rightarrow b\bar{b})$ of the exotic boson assuming a production cross section and decay branching ratio of the exotic boson as predicted by the SM for the Higgs boson. We also test the hypotheses of the exotic models by comparing the data with the predictions.

The CDF II detector is described in detail elsewhere [20, 21]. Silicon-strip tracking detectors [22] surround the interaction region and provide precise measurements of charged-particle trajectories in the range $|\eta| < 2$ [23]. A cylindrical drift chamber provides full coverage over the range $|\eta| < 1$. The tracking detectors are located within a 1.4 T superconducting solenoidal magnet with field oriented along the beam direction. The energies of individual particles and particle jets are measured in segmented electromagnetic and hadronic calorimeters arranged in a projective-tower geometry surrounding the solenoid. Tracking drift chambers and scintillation counters are located outside of the calorimeters to help identify muon candidates [24]. The Tevatron collider luminosity is measured with multilayer gas Cherenkov detectors [25]. The data set used in the analyses reported in this Letter corresponds to an integrated luminosity of 9.45 fb$^{-1}$. The data are collected using a three-level online event selection system (trigger). The first level, relying on special-purpose hardware [26], and the second level, using a mixture of dedicated hardware and fast software algorithms, reduce the event accept-rate to a level readable by the data acquisition system. The accepted events are processed online at the third trigger level with fast reconstruction algorithms, and recorded for offline analysis [27].

To predict the kinematic distributions of SM Higgs boson events, we use the PYTHIA [28] Monte Carlo (MC) program, with CTEQ5L [29] parton distribution functions (PDFs) of leading order (LO) in the strong coupling parameter $\alpha_s$. We scale these MC predictions to the highest-order cross section calculations available. To predict the exotic signal kinematic distributions, we use a modified version of MADEVENT [30] provided by the authors of Ref. [13].

The predictions for the SM WH and ZH cross sections [31] are based on the next-to-leading order (NLO) calculation of $V^2H$ [32] and include next-to-next-to-leading order (NNLO) quantum chromodynamical (QCD) contributions [33], as well as one-loop electroweak corrections [34]. In the predictions for the decay branching fractions of the SM Higgs boson [35, 36], the partial decay widths for all decays except to pairs of $W$ and $Z$ bosons are computed with HDECAY [37], and the $WW$ and $ZZ$ decay widths are computed with PROPHET4F [38]. The relevant rates are $\sigma_{WH} = (129.5 \pm 9.8)$ fb, $\sigma_{ZH} = (78.5 \pm 5.9)$ fb, and $B(H \rightarrow b\bar{b}) = (57.8 \pm 1.0)\%$. The uncertainties on the predicted branching ratio from uncertainties in the bottom-quark mass, $\alpha_s$, and missing higher-order effects are estimated in Refs. [39, 40].

We model SM processes and instrumental backgrounds using data-driven and MC methods. Simulated diboson ($WW$, $WZ$, $ZZ$) MC samples are normalized using the NLO calculations from MC@NLO [41]. For $tt$ we use a production cross section of $7.04 \pm 0.7$ pb [42], which is based on a top-quark mass of 173 GeV/$c^2$ and MSTW 2008 NNLO PDFs [43]. The single-top-quark production cross section is taken to be $3.15 \pm 0.31$ pb [44]. The normalization of the $Z+jets$ and $W+jets$ MC samples is taken from ALPGEN [45] corrected for NLO effects, except in
the case of the $WH \to \ell\nu b\bar{b}$ search. The normalization of the $W+\text{jets}$ MC sample in the $WH \to \ell\nu b\bar{b}$ search, and the normalization of the instrumental and QCD multijet samples in all searches, are constrained from data samples where the expected $s/b$ ratio is several orders of magnitude smaller than in the search samples. The quality of background modeling is shown in final-state invariant mass distribution plots included in the Supplemental Material to this Letter, which show good agreement with the data in all cases.

The analyses used to search for the exotic pseudoscalar and graviton-like Higgs bosons are modifications of the searches for the SM Higgs boson, optimized for separating the exotic signals from both the SM background sources and the possible SM Higgs boson signal. They use the most recent and efficient CDF algorithm, HOBIT [40], for identifying jets from the hadronization of bottom quarks ($b$-tagging). HOBIT is a multivariate classifier that uses kinematic properties of reconstructed trajectories of charged particles (tracks) associated with displaced vertices, the impact parameters of the tracks, and other characteristics of reconstructed groups of collimated particles (jets) that help separate $b$-jets from light-flavored jets. The HOBIT classifier does not perform well for jets with $E_T > 200$ GeV and the data-based calibration procedures associated with it suffer from greater uncertainties in this kinematic region. We therefore do not tag jets with $E_T > 200$ GeV. The same tight (T) and loose (L) tag requirements are used as in the SM Higgs analyses.

In each final state, the search channels are subdivided according to the number of jets, the lepton category, and the $b$-tag category. The $WX \to \ell\nu b\bar{b}$ events are divided into 15 subchannels, corresponding to the TT, TL, 1T, LL, and 1L tagging categories of the two jets, for each lepton category: central leptons (electrons or muons), forward electrons, and isolated-track leptons. The $ZX \to \ell^+\ell^-b\bar{b}$ events are divided into 16 subchannels, corresponding to the TT, TL, 1T, LL tagging categories in the two- and three-jet final states, separately for $Z \to e^+e^-$ and $Z \to \mu^+\mu^-$ events. The $WX+ZX \to E_T b\bar{b}$ events are divided into 6 subchannels corresponding to the TT, TL, and 1T tagging categories in 2-jet and 3-jet final states. A total of 37 analysis channels are defined. The expected and observed event yields in all channels are summarized in Table I, summed over lepton, jet, and $b$-tag categories.

| Process          | $\ell^+\ell^- b\bar{b}$ | $\ell\nu b\bar{b}$ | $E_T b\bar{b}$ |
|------------------|--------------------------|---------------------|----------------|
| $V + X_0^-$      | 81±1                     | 49±4               | 81±6           |
| $V + X_2^+$      | 7±1                      | 43±4               | 65±5           |
| $WH$             | 7±1                      | 33±3               | 40±3           |
| $V + \text{jets}$| 820±141                  | 23323±2860         | 9193±2273      |
| Dibosons         | 72±1                     | 1288±148           | 544±66         |
| Top              | 222±22                   | 2053±211           | 1935±164       |
| QCD              | 58±21                    | 2406±603           | 16283±1447     |
| Total bkg        | 1172±372                 | 29070±3037         | 27956±3188     |

To summarize the data in the large number of contributing channels, we follow Ref. [1]. We sum the contents of bins with similar $s/b$ ratios over the output histograms of all channels. Fig. [1] shows the comparison of the data with the best-fit background predictions and the summed signals, separately for the SM Higgs and exotic boson signals. The signal strength modifier is denoted by $\mu_{\text{exotic}}$, which multiplies the SM signal strength to predict the rate in the exotic model under test. Both distributions show agreement between the background predictions and the observed data over five orders of magnitude. No evidence for an excess of exotic signal-like candidates is seen.

A number of systematic uncertainties among the various analyses affect the sensitivity of the final result. All correlations within and between channels are taken into account in deriving the following combined limits, cross sections, and $p$-values. Uncertainties of 5% [31] on the inclusive $WH$ and $ZH$ production rates are estimated by varying the factorization and renormalization scales. We assign uncertainties to the Higgs boson branching ratios as calculated in Ref. [10]. Since the exotic signals are normalized to the SM Higgs cross section, the same relative uncertainties are assumed for the exotic production. The largest sources of uncertainty on the dominant backgrounds are the rates of $V+$heavy-flavor jets. The resulting uncertainties are up to 8% of the predicted values. Because the various analyses use different methods to obtain the $V+$heavy-flavor predictions, we treat their uncertainties as uncorrelated between the $\ell\nu b\bar{b}$, the $E_T b\bar{b}$, and $\ell^+\ell^- b\bar{b}$ channels. We use simulated events to study
The luminosity uncertainty is correlated between detector acceptance uncertainties and a 4.0% on the integrated luminosity is 6%, of which 4.4% originates from detector acceptance uncertainties and shapes of the signal and background expectations. We treat the jet-energy-scale variations uncorrelated among the three analyses in the combined search. The uncertainty on lepton identification and trigger efficiencies range from 2% to 6% and are applied to both signal and MC-based background predictions. The uncertainty on the integrated luminosity is 6%, of which 4.4% originates from detector acceptance uncertainties and 4.0% is due to the uncertainty on the inelastic $p\bar{p}$ cross section [49]. The luminosity uncertainty is correlated between the signal and MC-based background predictions.

Bayesian exclusion limits at 95% credibility level (C.L.) [50] on the production rates times the branching fraction $B(X \to bb)$ for $0^−$ and $2^+$ Higgs bosons are reported in Table III both separately for each channel and combined, in units of the SM Higgs boson production rate. The limits are computed from a likelihood defined as the product of the probability densities for the bin contents of the MVA histograms over all bins of each histogram and all channel histograms, assuming Poisson probability densities for the bin contents, uniform prior densities for the SM and exotic signal strength modifiers $\mu_{\text{exotic}}$ and $\mu_{\text{SM}}$, and Gaussian prior densities for the nuisance parameters describing systematic uncertainties. Posterior densities and upper limits on the SM and exotic Higgs boson rates are obtained from pseudo-experiments (PEs), where in each PE the likelihood is integrated over the nuisance parameters and then it is maximized. The medians of the distributions of results from PEs are used as the most probable values. The SM ratio between $WH$ and $ZH$ production rates is assumed when combining $WX$ and $ZX$ searches. Limits are listed either assuming that the SM Higgs boson is present as a background, or absent. Since the exotic $0^−$ and $2^+$ signals populate kinematic regions different from those of the SM Higgs boson, and since the SM Higgs boson production rate is small, the expected and observed limits on the exotic rates are very similar whether the SM Higgs boson is present or not. The observed combined limits are somewhat stronger than expected, with an exclusion rate of $\mu_{\text{exotic}} < 0.32$ in the $0^−$ case (approximately a one standard deviation deficit), and $\mu_{\text{exotic}} < 0.35$ in the $2^+$ case (approximately a two standard deviation deficit). The $E_Tbb$ channel carries the largest weight in the combination. A number of candidates somewhat lower than expected appear in the most signal-like bins of the exotic discriminants in this channel. The two-dimensional cross section fits, which allow for arbitrary rates of both SM and exotic Higgs bosons to be simultaneously present, are shown in Fig. 2 separately for the $0^−$ and $2^+$ searches.

![Graph](image-url)

**FIG. 1:** Distributions of $\log_{10}(s/b)$ for the data from all contributing Higgs boson search channels for a boson mass of 125 GeV/c² for (a) the $0^−$ search and (b) the $2^+$ search. The observed numbers of events are represented by the points, and the expected exotic signals are shown as histograms with $\mu_{\text{exotic}} = 1$ stacked on top of the backgrounds, which are fit to the data within their systematic uncertainties. The expected $s/b$ ratios of the exotic signal over the background yield are used to rank analysis bins. The background predictions do not include the contributions from the SM Higgs boson, which are shown as separate histograms, not stacked. The error bars shown on the data correspond to the square root of the observed data count. Underflows and overflows are collected into the leftmost and rightmost bins, respectively.

| Channel | Obs $0^−$ Median [limit/HSM] | Obs $2^+$ Median [limit/HSM] | Obs $0^−$ Median [limit/HSM] | Obs $2^+$ Median [limit/HSM] |
|---------|-----------------------------|-----------------------------|-----------------------------|-----------------------------|
| $\ell^+\ell^−bb$ | 0.59 (0.55) | 0.74 (0.78) | 1.05 (0.99) | 1.01 (1.03) |
| $\ell^+\ell^−bb$ | 1.15 (1.77) | 1.15 (1.52) | 1.57 (1.49) | 1.59 (1.61) |
| $E_Tbb$ | 0.32 (0.28) | 0.44 (0.45) | 0.35 (0.31) | 0.79 (0.83) |

**TABLE II:** Limits at 95% C.L. on $0^−$ and $2^+$ boson production assuming no SM Higgs boson background. In parentheses are the limits assuming SM Higgs boson background.

We report the observed values and the expected distributions of the log-likelihood ratio (LLR) [50] in the SM and the exotic hypotheses and list the combined results in Table III. The Table includes the $p$-values for the null and test hypotheses, defined as the conditional probabilities $P_{null} = P(\text{LLR} < \text{LLR}_{\text{obs}} | \text{SM})$ and $P_{test} = P(\text{LLR} > \text{LLR}_{\text{obs}} | \text{SM})$. 

We report the observed values and the expected distributions of the log-likelihood ratio (LLR) [50] in the SM and the exotic hypotheses and list the combined results in Table III. The Table includes the $p$-values for the null and test hypotheses, defined as the conditional probabilities $P_{null} = P(\text{LLR} < \text{LLR}_{\text{obs}} | \text{SM})$ and $P_{test} = P(\text{LLR} > \text{LLR}_{\text{obs}} | \text{SM})$.
events with different kinematic properties (high $M^2$ against the SM Higgs boson, as the exotic search tests for production. This deficit in the exotic search is not evidence for an admixture of SM production and exotic states, both allowing for an admixture of SM production and exotic

production, and assuming only exotic production.

Acknowledgments

We thank the Fermilab staff and the technical staffs of the participating institutions for their vital contributions. This work was supported by the U.S. Department of Energy and National Science Foundation; the Italian Istituto Nazionale di Fisica Nucleare; the Ministry of Education, Culture, Sports, Science and Technology of Japan; the Natural Sciences and Engineering Research Council of Canada; the National Science Council of the Republic of China; the Swiss National Science Foundation; the A.P. Sloan Foundation; the Bundesministerium für Bildung und Forschung, Germany; the Korean World Class University Program, the National Research Foundation of Korea; the Science and Technology Facilities Council and the Royal Society, United Kingdom; the Russian Foundation for Basic Research; the Ministerio de Ciencia e Innovación, and Programa Consolider-Ingenio 2010, Spain; the Slovak R&D Agency; the Academy of Finland; the Australian Research Council (ARC); and the EU community Marie Curie Fellowship Contract No. 302103.

FIG. 2: Combined two-dimensional posterior density of the measured (a) 0$^-$-vs.-0$^+$ and (b) 2$^+$-vs.-0$^+$ cross sections, normalized to the SM predictions.

$P_{\text{test}} = P(\text{LLR} \geq \text{LLR}_{\text{obs}}|\text{exotic})$, respectively, the values of $CL_\alpha = P_{\text{test}}/(1 - P_{\text{null}})$, and the equivalent number of Gaussian standard deviations $\sigma$ corresponding to each $p$-value, defined by $p = 1 - \text{erf}(z/\sqrt{2})/2$. There is a deficit in the observed number of events in the signal-like bins of the exotic discriminant, which is visible in Fig. 1 in both the 0$^-$ and the 2$^+$ searches. The dominant contribution to this deficit comes from the $WX + ZX \rightarrow E_T^\gamma b\bar{b}$ search. This deficit in the exotic search is not evidence against the SM Higgs boson, as the exotic search tests for events with different kinematic properties (high $M_{Vb\bar{b}}$) than those of the SM Higgs boson. Indeed, the combined cross section fit, shown in Fig. 2, is consistent with the SM Higgs boson rate with a discrepancy of less than 0.5 standard deviations.

In conclusion, we search in the entire CDF data sample for Higgs-boson-like particles of the same mass, production and decay modes, and production rates as the discovered SM Higgs boson candidate, but with 0$^-$ or 2$^+$ spin-parity quantum numbers. We observe no significant deviations from the SM predictions with a Higgs boson of mass $m_H \approx 125 \text{ GeV}/c^2$, and set bounds on the possible rate of production of 0$^-$ and 2$^+$ exotic states, both allowing for an admixture of SM production and exotic

$^*$ Deceased

1 With visitors from $^a$University of British Columbia, Vancouver, BC V6T 1Z1, Canada, $^b$Istituto Nazionale di Fisica Nucleare, Sezione di Cagliari, 09042 Monserrato (Cagliari), Italy, $^c$University of California Irvine, Irvine, CA 92697, USA, $^d$Institute of Physics, Academy of Sciences of the Czech Republic, 182 21, Czech Republic, $^e$CERN, CH-1211 Geneva, Switzerland, $^f$Cornell University, Ithaca, NY 14853, USA, $^g$University of Cyprus, Nicosia CY-1678, Cyprus, $^h$Office of Science, U.S. Department of Energy, Washington, DC 20585, USA, $^i$University College Dublin, Dublin 4, Ireland, $^j$ETH, 8092 Zürich, Switzerland, $^k$University of Fukui, Fukui City, Fukui Prefecture, Japan 910-0017, $^l$Universidad Iberoamericana, Lomas de Santa Fe, México, C.P. 01219, Distrito Federal, $^m$University of Iowa, Iowa City, IA 52242, USA, $^n$Kinki University, Higashi-Osaka City, Japan 577-8502, $^o$Kansas State University, Manhattan, KS 66506, USA, $^p$Brookhaven National Laboratory, Upton, NY 11973, USA, $^q$Istituto Nazionale di Fisica Nucleare, Sezione di Lecce, Via Arnesano, I-73100 Lecce, Italy, $^r$Queen Mary, University of London, London, E1 4NS, United Kingdom, $^s$University of Melbourne, Victoria 3010, Australia, $^t$Muons, Inc., Batavia, IL 60510, USA, $^u$Nagasaki Institute of Applied Science, Nagasaki 851-0193, Japan, $^v$National Research Nuclear University, Moscow 115409, Russia, $^w$Northwestern University, Evanston, IL 60208, USA, $^x$University of Notre Dame, Notre Dame, IN 46556, USA, $^y$Universidad de Oviedo, E-33007 Oviedo, Spain, $^z$CNRS-IN2P3, Paris, F-75205 France, $^{aa}$Universidad Tecnica Federico Santa Maria, 110v Valparaiso, Chile, $^{bb}$The University of Jordan, Amman 11942, Jordan, $^{cc}$Universite catholique de Louvain.
null significance $p_{\text{null}}$ reflects the deficit of signal-like events compared with the background prediction.

| $0^\circ$ | $2^\circ$ |
|----------|----------|
| LLR$_{\text{abs}}$ | 24.6 | 20.8 |
| LLR$_{\text{SM}}$, median | 13.2 | 9.5 |
| LLR$_{\text{exotic}}$, median | -15.5 | -10.8 |
| $p_{\text{null}}$ | 0.943 ($-1.58$ s.d.) | 0.967 ($-1.83$ s.d.) |
| Median expected $p_{\text{null}}$ (if exotic) | $3.87 \times 10^{-4}$ ($3.95$ s.d.) | $4.96 \times 10^{-4}$ ($3.29$ s.d.) |
| $p_{\text{test}}$ | $1.72 \times 10^{-7}$ ($5.10$ s.d.) | $7.65 \times 10^{-7}$ ($4.81$ s.d.) |
| Median expected $p_{\text{test}}$ (if SM) | $1.36 \times 10^{-4}$ ($3.64$ s.d.) | $1.01 \times 10^{-3}$ ($3.09$ s.d.) |
| $\text{CL}_a$ | $3.03 \times 10^{-5}$ ($4.52$ s.d.) | $2.29 \times 10^{-4}$ ($4.08$ s.d.) |
| Median expected $\text{CL}_a$ | $2.72 \times 10^{-4}$ ($3.46$ s.d.) | $2.01 \times 10^{-3}$ ($2.88$ s.d.) |
brock, Phys. Lett. B 273, 167 (1991).
[33] O. Brein, A. Djouadi, and R. Harlander, Phys. Lett. B 579, 149 (2004).
[34] M. L. Ciccolini, S. Dittmaier, and M. Kramer, Phys. Rev. D 68, 073003 (2003).
[35] S. Dittmaier et al. (LHC Higgs Cross Section Working Group Collaboration), arXiv:hep-ph/1101.0593.
[36] S. Dittmaier et al. (LHC Higgs Cross Section Working Group Collaboration), arXiv:hep-ph/1201.3084.
[37] A. Djouadi, J. Kalinowski, and M. Spira, Comput. Phys. Commun. 108, 56 (1998).
[38] A. Bredenstein, A. Denner, S. Dittmaier, and M. M. Weber, Phys. Rev. D 74, 013004 (2006); A. Bredenstein, A. Denner, S. Dittmaier, A. Mück, and M. M. Weber, J. High Energy Phys. 02 (2007) 080.
[39] J. Baglio and A. Djouadi, J. High Energy Phys. 03 (2011) 055.
[40] A. Denner, S. Heinemeyer, I. Puljak, D. Rebuzzi, and M. Spira, Eur. Phys. J. C 71, 1753 (2011).
[41] J. M. Campbell and R. K. Ellis, Phys. Rev. D 60, 113006 (1999).
[42] S. Moch and P. Uwer, Nucl. Phys. Proc. Suppl. 183, 75 (2008).
[43] A. D. Martin, W. J. Stirling, R. S. Thorne, and G. Watt, Eur. Phys. J. C 63, 189 (2009).
[44] N. Kidonakis, Phys. Rev. D 74, 114012 (2006).
[45] M. Mangano, M. Moretti, F. Piccinini, R. Pittau, and A. Polosa, J. High Energy Phys. 07 (2003) 001.
[46] J. Freeman, T. Junk, M. Kirby, Y. Oksuzian, T. J. Phillips, F. D. Snider, M. Trovato, J. Vizan, and W. M. Yao, Nucl. Instrum. Meth. A 697, 64 (2013)
[47] O. Brein, R. V. Harlander, M. Weisemann, and T. Zirke, Eur. Phys. J. C 72, 1868 (2012).
[48] A. Bhatti et al., Nucl. Instrum. Methods A 566, 375 (2006).
[49] S. Klimenko, J. Konigsberg, and T. M. Liss, FERMILAB-FN-0741 (2003).
[50] Statistics, in K. Nakamura et al. (Particle Data Group), J. Phys. G 37, 075021 (2010).
FIG. 3: $E_T b \bar{b}$ two-dimensional posterior density of the measured (a) $0^-\text{-vs-}0^+$ and (b) $2^+\text{-vs-}0^+$ cross sections, normalized to the SM predictions.

FIG. 4: $\ell \nu b \bar{b}$ two-dimensional posterior density of the measured (a) $0^-\text{-vs-}0^+$ and (b) $2^+\text{-vs-}0^+$ cross sections, normalized to the SM predictions.
FIG. 5: $\ell\ell\bar{b}b$ two-dimensional posterior density of the measured (a) $0^-\text{-vs.-}0^+$ and (b) $2^+\text{-vs.-}0^+$ cross sections, normalized to the SM predictions.

FIG. 6: $E_T\ell\bar{b}b$ LLR distributions for (a) $0^-$ and (b) $2^+$ hypotheses, assuming $\mu = 1$.

FIG. 7: $\ell\nu\bar{b}b$ LLR distributions for (a) $0^-$ and (b) $2^+$ hypotheses, assuming $\mu = 1$. 
FIG. 8: $\ell\ell\bar{b}\bar{b}$ LLR distributions for (a) $0^-$ and (b) $2^+$ hypotheses, assuming $\mu = 1$.

FIG. 9: Combined LLR distributions for (a) $0^-$ and (b) $2^+$ hypotheses, assuming $\mu = 1$.

FIG. 10: Background-subtracted distribution of the discriminant histograms, summed for bins with similar signal-to-background ratio ($s/b$) over all contributing Higgs boson search channels, for $m_H = 125$ GeV/$c^2$, for (a) the $0^-$ search and (b) the $2^+$ search. The background is fit to the data in each case, and the uncertainty on the background, shown with dashed lines, is after the fit. The exotic signal model, scaled to the SM Higgs boson expectation, is shown with a filled histogram. The SM Higgs boson expectation is also shown with a solid line. The error bars shown on the data points correspond in each bin to the square root of the sum of the expected signal and background yields. Underflows and overflows are collected into the leftmost and rightmost bins, respectively.
FIG. 11: Exclusion limits on the fraction of exotic boson in the total signal for the exotic + SM Higgs boson admixture hypotheses. The limits are shown as functions of the total signal production rate relative to the SM prediction for the Higgs boson rate.
FIG. 12: Discriminant function for (a) the tight-tight and (b) the tight-loose $b$-jet categories of the $\ell\nu b\bar{b}$ search channel for a $0^-$ state. Events are first categorized according to their exotic discriminant outputs. If these pass below a threshold of 0.5, then the SM discriminant function is used instead, scaled to the range $[0,0.5]$. In this way, kinematic regions that are the most sensitive to testing for the presence of an exotic Higgs boson are used first, and non-exotic-like events are used to compare the data with the SM Higgs boson hypothesis.

FIG. 13: Discriminant function for (a) the loose-loose and (b) the 1-tight (right) $b$-jet categories of the $\ell\nu b\bar{b}$ search channel for a $0^-$ state.

FIG. 14: Discriminant function for the 1-loose $b$-jet category of the $\ell\nu b\bar{b}$ search channel for a $2^+$ state.
FIG. 15: Discriminant function for (a) the tight-tight and (b) the tight-loose \( b \)-jet categories in the 2-jet bin of the \( \ell \ell \bar{b} \bar{b} \) search channel for a 0\(^{-} \) state.

FIG. 16: Discriminant function for (a) the loose-loose and (b) the 1-tight \( b \)-jet categories in the 2-jet bin of the \( \ell \ell \bar{b} \bar{b} \) search channel for a 0\(^{-} \) state.

FIG. 17: Discriminant function for (a) the tight-tight and (b) the tight-loose \( b \)-jet categories in the 3-jet bin of the \( \ell \ell \bar{b} \bar{b} \) search channel for a 0\(^{-} \) state.
FIG. 18: Discriminant function for (a) the loose-loose and (b) the 1-tight $b$-jet categories in the 3-jet bin of the $\ell\ell b\bar{b}$ search channel for a $0^-$ state.

FIG. 19: Discriminant function for (a) the tight-tight and (b) the tight-loose $b$-jet categories in the 2-jet bin of the $E_T b\bar{b}$ search channel for a $0^-$ state. Events are first categorized according to their exotic discriminant outputs. If these pass below a threshold (typically 0.5 on a scale of 0 to 1), then the SM discriminant function is used instead, scaled to the range [0,0.5]. In this way, kinematic regions that are the most sensitive to testing for the presence of an exotic Higgs boson are used first, and non-exotic-like events are used to compare the data with the SM Higgs boson hypothesis.

FIG. 20: Discriminant function for the 1-tight $b$-jet category in the 2-jet bin of the $E_T b\bar{b}$ search channel for a $0^-$ state.
FIG. 21: Discriminant function for (a) the tight-tight and (b) the tight-loose $b$-jet categories in the 3-jet bin of the $E_T^{bb}$ search channel for a $0^-$ state.

FIG. 22: Discriminant function for the 1-tight $b$-jet category in the 3-jet bin of the $E_T^{bb}$ search channel for a $0^-$ state.
FIG. 23: Discriminant function for (a) the tight-tight and (b) the tight-loose $b$-jet categories of the $\ell\nu b\bar{b}$ search channel for a $2^+$ state. Events are first categorized according to their exotic discriminant outputs. If these pass below a threshold of 0.5, then the SM discriminant function is used instead, scaled to the range [0, 0.5]. In this way, kinematic regions that are the most sensitive to testing for the presence of an exotic Higgs boson are used first, and non-exotic-like events are used to compare the data with the SM Higgs boson hypothesis.

FIG. 24: Discriminant function for (a) the loose-loose and (b) the 1-tight $b$-jet categories of the $\ell\nu b\bar{b}$ search channel for a $2^+$ state.

FIG. 25: Discriminant function for the 1-loose $b$-jet category of the $\ell\nu b\bar{b}$ search channel for a $2^+$ state.
FIG. 26: Discriminant function for (a) the tight-tight and (b) the tight-loose $b$-jet categories in the 2-jet bin of the $\ell\ell b\bar{b}$ search channel for a $2^+$ state.

FIG. 27: Discriminant function for (a) the loose-loose and (b) the 1-tight $b$-jet categories in the 2-jet bin of the $\ell\ell b\bar{b}$ search channel for a $2^+$ state.

FIG. 28: Discriminant function for (a) the tight-tight and (b) the tight-loose $b$-jet categories in the 3-jet bin of the $\ell\ell b\bar{b}$ search channel for a $2^+$ state.
FIG. 29: Discriminant function for (a) the loose-loose and (b) the 1-tight (right) b-jet categories in the 3-jet bin of the $\ell\ell b\bar{b}$ search channel for a $2^+$ state.

FIG. 30: Discriminant function for (a) the tight-tight and (b) the tight-loose b-jet categories in the 2-jet bin of the $\not{E}_T b\bar{b}$ search channel for a $2^+$ state. Events are first categorized according to their exotic discriminant outputs. If these pass below a threshold of 0.6, then the SM discriminant function is used instead, scaled to the range [0,0.5]. In this way, kinematic regions that are the most sensitive to testing for the presence of an exotic Higgs boson are used first, and non-exotic-like events are used to compare the data with the SM Higgs boson hypothesis.

FIG. 31: Discriminant function for the 1-tight b-jet category in the 2-jet bin of the $\not{E}_T b\bar{b}$ search channel for a $2^+$ state.
FIG. 32: Discriminant function for (a) the tight-tight and (b) the tight-loose $b$-jet categories in the 3-jet bin of the $E_T^{bb}$ search channel for a $2^+$ state.

FIG. 33: Discriminant function for the 1-tight $b$-jet category in the 3-jet bin of the $E_T^{bb}$ search channel for a $2^+$ state.
FIG. 34: Reconstructed $Vb\bar{b}$ transverse invariant mass distribution for (a) the tight-tight and (b) the tight-loose $b$-jet categories of the $\ell\nu b\bar{b}$ search channel.

FIG. 35: Reconstructed $Vb\bar{b}$ transverse invariant mass distribution for (a) the loose-loose and (b) the 1-tight $b$-jet categories of the $\ell\nu b\bar{b}$ search channel.

FIG. 36: Reconstructed $Vb\bar{b}$ transverse invariant mass distribution for the 1-loose $b$-jet category of the $\ell\nu b\bar{b}$ search channel.
FIG. 37: Reconstructed $Vb\bar{b}$ invariant mass distribution for (a) the tight-tight and (b) the tight-loose (right) $b$-jet categories in the 2-jet bin of the $\ell\ell b\bar{b}$ search channel.

FIG. 38: Reconstructed $Vb\bar{b}$ invariant mass distribution for (a) the loose-loose and (b) the 1-tight $b$-jet categories in the 2-jet bin of the $\ell\ell b\bar{b}$ search channel.

FIG. 39: Reconstructed $Vb\bar{b}$ invariant mass distribution for (a) the tight-tight (left) and (b) the tight-loose $b$-jet categories in the 3-jet bin of the $\ell\ell b\bar{b}$ search channel.
FIG. 40: Reconstructed $Vb\bar{b}$ invariant mass distribution for (a) the loose-loose (left) and (b) the 1-tight $b$-jet categories in the 3-jet bin of the $\ell\ell b\bar{b}$ search channel.

FIG. 41: Reconstructed $Vb\bar{b}$ transverse invariant mass distribution for (a) the tight-tight and (b) the tight-loose $b$-jet categories in the 2-jet bin of the $E_T b\bar{b}$ search channel.

FIG. 42: Reconstructed $Vb\bar{b}$ transverse invariant mass distribution for the 1-tight $b$-jet category in the 2-jet bin of the $E_T b\bar{b}$ search channel.
FIG. 43: Reconstructed $Vb\bar{b}$ transverse invariant mass distribution for (a) the tight-tight and (b) the tight-loose $b$-jet categories in the 3-jet bin of the $E_Tb\bar{b}$ search channel.

FIG. 44: Reconstructed $Vb\bar{b}$ transverse invariant mass distribution for the 1-tight $b$-jet category in the 3-jet bin of the $E_Tb\bar{b}$ search channel.
FIG. 45: Reconstructed $b\bar{b}$ invariant mass distribution for (a) the tight-tight and (b) the tight-loose $b$-jet categories of the $\ell\nu b\bar{b}$ search channel. Overflows are added to the content of the uppermost bin.

FIG. 46: Reconstructed $b\bar{b}$ invariant mass distribution for (a) the loose-loose and (b) the 1-tight $b$-jet categories of the $\ell\nu b\bar{b}$ search channel. Overflows are added to the content of the uppermost bin.

FIG. 47: Reconstructed $b\bar{b}$ invariant mass distribution for the 1-loose $b$-jet category of the $\ell\nu b\bar{b}$ search channel. Overflows are added to the content of the uppermost bin.
FIG. 48: Reconstructed $b\bar{b}$ invariant mass distribution for (a) the tight-tight and (b) the tight-loose $b$-jet categories in the 2-jet bin of the $\ell\ell b\bar{b}$ search channel.

FIG. 49: Reconstructed $b\bar{b}$ invariant mass distribution for (a) the loose-loose and (b) the 1-tight $b$-jet categories in the 2-jet bin of the $\ell\ell b\bar{b}$ search channel.

FIG. 50: Reconstructed $b\bar{b}$ invariant mass distribution for (a) the tight-tight and (b) the tight-loose $b$-jet categories in the 3-jet bin of the $\ell\ell b\bar{b}$ search channel.
FIG. 51: Reconstructed $b\bar{b}$ invariant mass distribution for (a) the loose-loose and (b) the 1-tight $b$-jet categories in the 3-jet bin of the $\ell\ell b\bar{b}$ search channel.

FIG. 52: Reconstructed $b\bar{b}$ invariant mass distribution for (a) the tight-tight and (b) the tight-loose $b$-jet categories in the 2-jet bin of the $E_T b\bar{b}$ search channel.

FIG. 53: Reconstructed $b\bar{b}$ invariant mass distribution for the 1-tight $b$-jet category in the 2-jet bin of the $E_T b\bar{b}$ search channel.
FIG. 54: Reconstructed $b\bar{b}$ invariant mass distribution for (a) the tight-tight and (b) the tight-loose $b$-jet categories in the 3-jet bin of the $E_T$ $b\bar{b}$ search channel.

FIG. 55: Reconstructed $b\bar{b}$ invariant mass distribution for the 1-tight $b$-jet category in the 3-jet bin of the $E_T$ $b\bar{b}$ search channel.