Comparison between PtCO\textsubscript{2} and PaCO\textsubscript{2} and Derived Parameters in Heart Failure Patients during Exercise: A Preliminary Study

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Abstract: Evaluation of arterial carbon dioxide pressure (PaCO\textsubscript{2}) and dead space to tidal volume ratio (V\textsubscript{D}/V\textsubscript{T}) during exercise is important for the identification of exercise limitation causes in heart failure (HF). However, repeated sampling of arterial or arterialized ear lobe capillary blood may be clumsy. The aim of our study was to estimate PaCO\textsubscript{2} by means of a non-invasive technique, transcutaneous PCO\textsubscript{2} (PtCO\textsubscript{2}), and to verify the correlation between PtCO\textsubscript{2} and PaCO\textsubscript{2} and between their derived parameters, such as V\textsubscript{D}/V\textsubscript{T}, during exercise in HF patients. 29 cardiopulmonary exercise tests (CPET) performed on a bike with a ramp protocol aimed at achieving maximal effort in ≈10 min were analyzed. PaCO\textsubscript{2} and PtCO\textsubscript{2} values were collected at rest and every 2 min during active pedaling. The uncertainty of PCO\textsubscript{2} and V\textsubscript{D}/V\textsubscript{T} measurements were determined by analyzing the error between the two methods. The accuracy of PtCO\textsubscript{2} measurements vs. PaCO\textsubscript{2} decreases towards the end of exercise. Therefore, a correction to PtCO\textsubscript{2} that keeps into account the time of the measurement was implemented with a multiple regression model. PtCO\textsubscript{2} and V\textsubscript{D}/V\textsubscript{T} changes at rest and at low exercise intensity. At high exercise intensity the overall response appears delayed but reproducible and the error can be overcome by mathematical modeling allowing an accurate estimation by PtCO\textsubscript{2} of PaCO\textsubscript{2} and V\textsubscript{D}/V\textsubscript{T}.

Keywords: biomedical instrumentation; heart failure; exercise; transcutaneous PCO\textsubscript{2}; arterial PCO\textsubscript{2}; V\textsubscript{D}/V\textsubscript{T}

1. Introduction

Assessment of dead space/tidal volume ratio (V\textsubscript{D}/V\textsubscript{T}) and PaCO\textsubscript{2} during exercise is of paramount importance for identification of exercise limitation at cardiopulmonary exercise testing (CPET) in the setting of several cardiovascular and pulmonary diseases, including heart failure (HF). V\textsubscript{D}/V\textsubscript{T} value during exercise is calculated through simultaneous measurement of PaCO\textsubscript{2} and mean expiratory PCO\textsubscript{2} (PtCO\textsubscript{2}) \cite{1}. V\textsubscript{D}/V\textsubscript{T} is used to assess ventilation/perfusion mismatch \cite{2,3} and it is elevated in case of concomitant pulmonary hypertension and/or respiratory disease. PaCO\textsubscript{2} value during the isocapnic...
buffering period is a recognized index of reflex ventilation regulation \[4,5\]. Moreover, the end tidal CO$_2$—arterial CO$_2$ pressure gradient (ΔPetCO$_2$ – PaCO$_2$) during exercise is another parameter useful to assess ventilation perfusion mismatch in the lung \[6\].

Repeated arterial or capillary ear lobe blood sampling, both in static conditions and during exercise, to measure/estimate PaCO$_2$ may be uneasy on a routine basis and outside of clinical settings. The technical reasons behind this are invasiveness, size of the catheter, instability of the calibration due to clotting, possible air contamination of the arterial blood sample and lack of reusability \[7,8\]. Therefore, non-invasive derived PaCO$_2$ estimation seems desirable. End-tidal PCO$_2$ (PetCO$_2$) has been considered as a reliable estimate of arterial PCO$_2$, in healthy subjects and in particular conditions such as monitoring during anesthesia \[9,10\]. However, increase in ventilation/perfusion mismatch makes evaluation of PaCO$_2$ by PetCO$_2$ highly unreliable in several diseases \[11–14\], as well as during sleep \[15\]. Moreover, a lack of accuracy in the estimation of PaCO$_2$ and $V_D/V_T$ by PetCO$_2$ has been reported during exercise making its use unreliable, at least in cardiorespiratory patients \[16\]. Regardless, albeit such an approximation is inaccurate, several commercial ergospirometers software report estimations of $V_D/V_T$ using PetCO$_2$ as a PaCO$_2$ surrogate \[17\].

Transcutaneous PCO$_2$ (PtCO$_2$) devices provide another option for the continuous noninvasive estimation of PaCO$_2$, overcoming the limitations posed by end-tidal CO$_2$ analysis \[18\]. PtCO$_2$ is measured using Severinghaus–Stow-type electrodes, i.e., with an electrochemical sensor \[19\], with a heating system that brings the skin temperature up to about 42 °C. Commercial devices include probes with a single PtCO$_2$ sensor, probes with a combination of partial pressure of oxygen (PO$_2$) and PtCO$_2$ and probes with a combination of pulse oximetry (SpO$_2$) and PtCO$_2$ measurements \[20\]. The methodology has been constantly improved over the years, making PtCO$_2$ systems easier to use and more reliable in clinical practice. The main characteristics of commercial sensors are small dimensions (diameter 15 mm, height 8 mm), long-time for re-membranization (every 2 weeks), calibration required twice a day, short arterIALIZation time (3 min) and high measurement reliability thanks to the protection of the membrane. This type of measurement has shown to closely approximate PaCO$_2$ both at rest and during symptom limited exercise in normal subjects and in patients with lung disease \[16\]. Whether PtCO$_2$ can be used as a reliable surrogate of PaCO$_2$ during a maximal effort in patients with heart failure is actually unknown. The aim of our study was therefore to verify the correlation between PtCO$_2$ and PaCO$_2$ and between $V_D/V_T$ derived from PtCO$_2$ and that derived from PaCO$_2$ during a maximal exercise test in patients with stable heart failure. The novelty of this study consists in the application of such electrochemical sensors, which require stable operational conditions, in a highly dynamic situation where parameters are expected to change faster, and movement artefacts might be present. The final purpose of the study is to find an adequate protocol to use PtCO$_2$ sensing on patients in dynamic conditions to estimate PaCO$_2$ and derived parameters, such as $V_D/V_T$. Using such a protocol allows to study the response to exercise, i.e., to an increased metabolic demand, with a continuous sampling and a non-invasive method.

2. Materials and Methods

This study was designed as a sub study of a larger trial (Ethics Committee approval number CCM966) dedicated to the analysis of exercise performance in patients with severe HF. Study inclusion criteria were stable chronic heart failure with stabilized therapy in NYHA class II or III; left ventricular ejection fraction ≤ 40%, peak oxygen uptake (VO$_2$) ≤ 12 mL/Kg/min or E/e’ > 13 at cardiac ultrasound and ability to perform a maximal exercise test on a bike. Exclusion criteria were age < 18 years, severe primitive valvular disease, significant pericardial disease, previous pulmonary embolism, peripheral arterial disease limiting exercise capacity, effort angina, or sign of ischemia at EKG, uncontrolled arrhythmias, pregnancy, severe pulmonary disease and the presence of any counterindication to exercise testing.
2.1. Procedures

A symptoms-limited maximal CPET was performed on a bike with a personalized ramp protocol (Quark PFT, Cosmed Cart, Rome, Italy) aimed to reach the maximal effort in around 10 min. The duration of the test was chosen based on the results by Agostoni et al. [21], who demonstrated that to assess exercise performance in HF patients by cardiopulmonary exercise test the exercise protocol needs to be 10 min long. To do so, the exercise protocol needs to be performed with a personalized progressive workload which means that the protocol must be adapted to the patient’s clinical conditions. Other types of protocols such as endurance or fixed workload or step increasing protocols do not allow to identify peak VO\textsubscript{2}. CPET was performed and analyzed following standard technique [22]. Briefly, patients were encouraged to continue the test until reaching a respiratory exchange ratio (RER) of at least 1.05. VO\textsubscript{2}, CO\textsubscript{2} production (VCO\textsubscript{2}), PetCO\textsubscript{2}, end tidal oxygen pressure (PetO\textsubscript{2}), ventilation (VE), tidal volume (V\textsubscript{T}), respiratory rate (RR) and workload were recorded breath by breath and averaged every 10 s. Several minutes before the exercise test a small catheter was inserted in the radial artery. Arterial blood samples were collected at rest, i.e., beginning of the loaded pedaling, (minute 0) and every 2 min during exercise and immediately analyzed by a blood gas analyzer (GEM Premier 4000, Werfen, Barcelona, Spain) for PaCO\textsubscript{2} determination. Heart rate (HR), hemoglobin O\textsubscript{2} saturation (SpO\textsubscript{2}) and PtCO\textsubscript{2} were monitored continuously. To measure PtCO\textsubscript{2}, a commercial electrochemical sensor combined with a heating system (V-sign™ Sensor 2, Sentec AG, Therwil, Switzerland) was used. The technical characteristics of the commercial measurement system used are reported in Table 1.

**Table 1.** Technical characteristics of the PtCO\textsubscript{2} sensor as reported in the user manual.

| Parameter                          | Value                                      |
|------------------------------------|--------------------------------------------|
| Measurement range                  | 0–200 mmHg (0–26.7 kPa)                    |
| Resolution                         | 0.1 mmHg (0.01 kPa) below 100 mmHg (10 kPa) |
|                                    | 1 mmHg (0.1 kPa) above 100 mmHg (10 kPa)   |
| Drift                              | Typically < 0.5%/h                        |
|                                    | <75 s                                      |
| Response time (T90)                |                                            |
| Linearity                          | Typically < 1 mmHg (0.13 kPa)              |
|                                    | Negligible                                 |
| Interference by anesthetic gases   | After sensor application or occurrence of a PtCO\textsubscript{2} artifact, PtCO\textsubscript{2} is displayed in grey until it (re)stabilizes |
| Stabilization/artifact detection   |                                            |

The PCO\textsubscript{2} measurement of the V-sign™ Sensor 2 is based on a Stow–Severinghaus type PCO\textsubscript{2} sensor, i.e., a thin electrolyte layer is confined to the sensor surface with a hydrophobic, CO\textsubscript{2} and O\textsubscript{2} permeable membrane. The system was calibrated and applied over the patient’s earlobe through a clip with an adhesive layer after application of a fluid drop for optimal contact to the skin.

PtCO\textsubscript{2} recording started after a stabilization time of around 10 min. A marker was applied at the time of arterial sample collection to synchronize PtCO\textsubscript{2}, PetCO\textsubscript{2} and PaCO\textsubscript{2} values. The V-sign™ Sensor 2 is known to have a response time <75 s, as reported in the user manual and in Table 1. Blood pressure was manually measured every two minutes by a sphygmomanometer. We analyzed data at rest, every two minutes of exercise and at the end of the ramp protocol. Since the loaded exercise started at 0 Watts no unloaded pedaling was done.

A total of 23 patients were enrolled in the present study, 6 of which have repeated the protocol twice, after treatment update. Overall, 29 acquisitions have been evaluated. The present study is a preliminary study, designed as a sub-study of a different research report. We were not able to define a priori the sample needed to define at each exercise step the reliability of PtCO\textsubscript{2} measurements because no data exist to predict such a difference. For
this reason, we used all measurements available from the original trial. The present report data may be used as reference for sample size determination on future studies on this topic.

### 2.2. Multiple Regression

As explained in detail in the following sections, it was observed (Figure 1) that the accuracy of PtCO2 measurements with respect to the reference PaCO2 values decreases at increasing timestamps, i.e., towards the end of the protocol. For this reason, the possibility of adding a correction to PtCO2 that keeps into account the time of the measurement during the protocol was exploited.

**Figure 1.** Mean values of PaCO2, PtCO2 and end-tidal CO2 partial pressure (PetCO2) at different timestamps. PetCO2 is shown for completeness of CO2 measurement parameters. 29 sets of data were available at minute 0, 2 and 4, 28 at min 6, 26 at min 8 and 22 at min 10.

This was implemented by means of a multiple regression model. Multiple regression is an extension of linear regression and is used to predict the value of a variable based on two or more inputs [23]; the general formula describing multiple regression is (1):

$$\hat{Y} = b_0 + \sum_{i=1}^{m} b_i X_i$$

where \(m\) is the number of input variables, \(\hat{Y}\) is the predicted output, \(b_i\) are the coefficients of the model (\(b_0\) is the value when all input variables are zero) and \(X_i\) are the input variables.

In this case, the value to be predicted is PaCO2 and the two variables that are used are PtCO2 and the timestamp (0 min, 2 min, 4 min, 6 min, 8 min, and 10 min). A corrected PtCO2 value is obtained afterwards, and this new value is compared to the previous results; the used formulation is given by (2):

$$Corrected \text{ PtCO2} = f(\text{PtCO2}, t) = 4.13 - 0.197 \cdot (t - t_0) + 0.873 \cdot \text{PtCO2}$$

In (2), \(t\) is a continuous variable expressed in min and \(t_0\) is the beginning of the loaded pedaling in the ramp protocol. The function \(f\) is given by the multiple regression model, which was developed with a Python software based on the library scikit-learn [24].

### 2.3. Uncertainty of PtCO2 and VD/VT Measurements

A first analysis consisted in estimating the uncertainty of PtCO2 and VD/VT measurements obtained at different measuring times (0 min, 2 min, 4 min, 6 min, 8 min and 10 min) by analyzing the error between the two measurement methods: PaCO2 vs. PtCO2 and VD/VT obtained from PaCO2 versus VD/VT obtained from PtCO2.
Then, a multiple regression was applied to PtCO$_2$ values at different timestamps to improve the measurements; the obtained values are referred to as corrected PtCO$_2$. The formulas to compute the error of PtCO$_2$ and corrected PtCO$_2$ are, respectively, (3) and (4):

\[
\text{Error before correction} \ (t - t_0) = \text{PtCO}_2(t - t_0) - \text{PaCO}_2(t - t_0) \quad (3)
\]
\[
\text{Error after correction} \ (t - t_0) = \text{corrected PtCO}_2(t - t_0) - \text{PaCO}_2(t - t_0) \quad (4)
\]

where \( t \) is a continuous variable expressed in minutes, \( t_0 \) is the beginning of the loaded pedaling in the ramp protocol and their difference is the timestamp at which the measurement is performed.

Bland–Altman plots [25,26], also known as Tukey mean-difference plots [27] in fields other than medicine and biosciences, were used to assess the agreement between the two measurement methods before and after the correction by multiple regression was applied.

In the case of V$_D$/V$_T$, the estimation of the parameters is analyzed when each PCO$_2$ value (arterial, non-corrected transcutaneous or corrected transcutaneous) is used, and the error is computed with the same method. In the present work, estimations of V$_D$/V$_T$ are performed with the Enghoff equation, i.e., using PaCO$_2$, instead of the Bohr equation because the latter uses alveolar CO$_2$ (PaCO$_2$) [28]. P$_E$CO$_2$ is the mean expiratory partial pressure of CO$_2$ and was obtained from cardiopulmonary exercise testing (CPET). The formulas to obtain V$_D$/V$_T$ in the different cases are (5)–(7):

\[
\frac{V_D}{V_T} \ (t - t_0) \ \text{from PaCO}_2 = 1 - \frac{P_E\text{CO}_2(t - t_0)}{\text{PaCO}_2(t - t_0)} \quad (5)
\]
\[
\frac{V_D}{V_T} \ (t - t_0) \ \text{from PtCO}_2 = 1 - \frac{P_E\text{CO}_2(t - t_0)}{\text{PtCO}_2(t - t_0)} \quad (6)
\]
\[
\frac{V_D}{V_T} \ (t - t_0) \ \text{from corrected PtCO}_2 = 1 - \frac{P_E\text{CO}_2(t - t_0)}{\text{corrected PtCO}_2(t - t_0)} \quad (7)
\]

2.4. Analysis of the Deltas

Another characteristic that is important to evaluate is the ability of the transcutaneous measurement system to follow differential variations of the value during the protocol. For this reason, variations of the values at 6, 8, and 10 min with respect to 2 min have been evaluated before and after the correction of PtCO$_2$ is applied. This was applied both in the case of PCO$_2$ and V$_D$/V$_T$ extracted from transcutaneous measurements. The 2-min blood sample was chosen due to its lower variability.

The distributions of the deltas of PtCO$_2$ and corrected PtCO$_2$ are compared pairwise with the deltas of PaCO$_2$; in the case of V$_D$/V$_T$, the deltas of the estimations obtained with PtCO$_2$ and corrected PtCO$_2$ are compared pairwise with the deltas of the estimations obtained from PaCO$_2$. PCO$_2$ deltas are expressed in mmHg, while V$_D$/V$_T$ deltas are adimensional.

2.5. Statistical Analysis

The distributions of the errors at different timestamps were analyzed with One-way repeated measurement ANOVA or an equivalent method for non-normal distributions. This method was chosen due to the repeated and correlated nature of the measurements. The comparison was performed considering minute 0 as the reference distribution in the case of PtCO$_2$ and the derived V$_D$/V$_T$.

The pairings of the deltas were first tested for normality with the Kolmogorov-Smirnov test [29]: for normal distributions, the paired t-test was used; for non-normal distributions, the Wilcoxon signed rank test was chosen instead.
3. Results

29 sets of data were available at minute 0, 2 and 4, 28 at minute 6, 26 at minute 8 and 22 at minute 10. Main clinical characteristics of the patients and main CPET results are reported in Table 2.

Table 2. Heart failure patient characteristics. Six subjects were tested twice. CPET data refer to 29 measurements. BMI = body mass index; CPET = cardiopulmonary exercise testing; VO\(_2\) = oxygen uptake; VE = ventilation; VCO\(_2\) = carbon dioxide production; RER = respiratory exchange ratio.

| Characteristic                                              | Mean ± SD |
|-------------------------------------------------------------|-----------|
| Age (years)                                                 | 69 ± 8    |
| Sex (M/F)                                                   | 22/1      |
| BMI                                                         | 26.4 ± 4.6|
| Heart failure etiology (primitive/ischemic)                 | 14/9      |
| Ejection fraction (%)                                        | 27.5 ± 9.9|
| Atrial fibrillation (Yes/No)                                | 11/12     |
| Peak VO\(_2\) (ml/kg/min)                                   | 12.2 ± 3.7|
| Peak VO\(_2\) (%)                                           | 53 ± 15   |
| VO\(_2\)/Work slope (ml/min/watt)                           | 7.9 ± 2.1 |
| VE/VCO\(_2\) slope                                          | 43.7 ± 10.9|
| Peak RER                                                    | 1.09 ± 0.09|
| Peak heart rate (bpm)                                       | 95 ± 25   |

3.1. Uncertainty of PtCO\(_2\) Measurements

In Figure 2, the boxplots of the errors in PaCO\(_2\) estimation before (left) and after PtCO\(_2\) is corrected (right) are reported. PtCO\(_2\) without correction tends to overestimate PaCO\(_2\) for high timestamps, while the error is stably centered around 0 after correction is applied.

![Figure 2](image-url)

Figure 2. Boxplots of the measurement errors of PtCO\(_2\) (left) and corrected PtCO\(_2\) (right) at different timestamps with respect to PaCO\(_2\).

The Bland–Altman analysis before and after correction is reported in Figures 3 and 4, respectively. In both cases, the difference is computer as (non-corrected or corrected) PtCO\(_2\) minus PaCO\(_2\).

The results of the One-way repeated measurements ANOVA or equivalent test for non-normal distributions are different before and after the correction with multiple regressions is performed.
Before the correction, the distributions are not normal. According to the Bonferroni t-tests (multiple comparisons vs. a control group, in this case the baseline), the distribution of the error after 10 min is significantly different from the minute 0 distribution \( (p = 0.011) \), while the distributions at other timestamps (2, 4, 6 and 8 min) have a \( p \)-value > 0.05.

After the correction, the distributions are normal. The differences in the mean values among the groups are not great enough to exclude the possibility that the difference is due to random sampling variability; there is not a statistically significant difference \( (p = 0.978) \).

3.2. Uncertainty of \( \frac{V_D}{V_T} \) Measurements Derived from PtCO\(_2\)

In Figure 5, the boxplots of the errors in \( \frac{V_D}{V_T} \) estimation from PtCO\(_2\) before (left) and after PtCO\(_2\) is corrected (right) are reported. Similar to PCO\(_2\), \( \frac{V_D}{V_T} \) calculated with PtCO\(_2\) without correction tends to overestimate \( \frac{V_D}{V_T} \) calculated with PaCO\(_2\) for high timestamps, while the error is stably centered around 0 after correction is applied.

Additionally in this case, the results of the One-way repeated measurements ANOVA or equivalent test for non-normal distributions are different before and after the correction of PtCO\(_2\) with multiple regressions is performed.
Before the correction, the distributions are not normal. According to the Bonferroni t-tests (multiple comparisons versus a control group, in this case the baseline), the distribution of the error after 10 min is significantly different from the minute 0 distribution ($p < 0.001$), while the distributions at other timestamps (2, 4, 6 and 8 min) have a $p$-value $> 0.05$.

After the correction, the distributions are still not normal. The differences in the mean values among the groups are not great enough to exclude the possibility that the difference is due to random sampling variability; there is not a statistically significant difference ($p = 0.864$).

### 3.3. Analysis of the Deltas

In Figure 6, the deltas of PaCO$_2$, PtCO$_2$ and corrected PtCO$_2$ at different timestamps with respect to the values measured after 2 min are reported.

The results of the statistical analysis are reported in Table 3. Deltas with respect to 2 min have been considered. The deltas are evaluated at 6, 8 and 10 min with respect to the values measured after 2 min. 28 pairs of data were available at minute 6, 26 at minute 8 and 22 at minute 10. The values in italic are those where the distribution is not normal. The values in bold are those with a $p$-value $< 0.05$ which highlights a statistically significant difference.
Table 3. p-values after the pairwise comparisons of deltas of PtCO₂ and corrected PtCO₂ with respect to deltas of PaCO₂.

|                      | Delta after 6 min | Delta after 8 min | Delta after 10 min |
|----------------------|-------------------|-------------------|-------------------|
| PaCO₂ vs. PtCO₂      | 0.099             | 0.022             | 0.023             |
| PaCO₂ vs. corrected PtCO₂ | 0.686             | 0.616             | 0.406             |

Without the correction by means of multiple regressions, there are statistically significant differences between the deltas at 8 and 10 min with respect to the measurements obtained after 2 min. The correction allows to remove such difference. Furthermore, the distributions after the correction are normal.

The same analysis was repeated for $V_D/V_T$. In Figure 7, the deltas of $V_D/V_T$ estimated with PaCO₂, PtCO₂ and corrected PtCO₂ at different timestamps with respect to the values measured after 2 min are reported while the overall results of the statistical analysis are reported in Table 4. The deltas are evaluated at 6, 8 and 10 min with respect to the values measured after 2 min. The values in bold are those with a $p$-value < 0.05 which highlights a statistically significant difference.

Figure 7. Boxplots of the deltas of $V_D/V_T$ estimated with PaCO₂, PtCO₂ and corrected PtCO₂. The deltas are evaluated at 6, 8 and 10 min with respect to the values measured after 2 min.

Table 4. p-values after the pairwise comparisons of deltas obtained with $V_D/V_T$ estimated with PtCO₂ and corrected PtCO₂ with respect to deltas of $V_D/V_T$ estimated with PaCO₂.

|                      | Delta after 6 min | Delta after 8 min | Delta after 10 min |
|----------------------|-------------------|-------------------|-------------------|
| $V_D/V_T$ estimated with PaCO₂ vs. PtCO₂ | 0.192             | 0.037             | 0.008             |
| $V_D/V_T$ estimated with PaCO₂ vs. corrected PtCO₂ | 0.990             | 0.818             | 0.332             |

Deltas with respect to the value measured 2 min after the beginning of the protocol have been considered. In this case, all distributions are normal, so the only used test was the paired t-test. Without the correction by means of multiple regressions, there are statistically significant differences between the deltas at 8 and 10 min with respect to the measurements obtained after 2 min. The correction allows to remove such difference in all cases.

4. Discussion

It is known from the literature that physiological parameters change with different levels of activity both inside and outside clinical settings [30,31] and that, at the same time, the performance of sensors and instrumentation in detecting these changes decreases with
increasing levels of activity [32]. For this reason, it is relevant to study the performance of different types of instrumentation also during experimental protocols with highly dynamic activities and maximal exercise. The present study shows that in patients with severe but stable heart failure PtCO$_2$ without any further correction is a reliable estimation of PaCO$_2$ at rest and during a progressive workload exercise only at low exercise intensity. Indeed, when exercise effort increases and PaCO$_2$ reduces the PCO$_2$ value derived by transcutaneous sensors show a delayed response. This delayed response is partly due to the delay of the sensor system, which is known to be <75 s; however, it must be noted that even if the PtCO$_2$ were partially shifted to take into account the delay, this correction would not be sufficient. Nevertheless, the overall response appears reproducible and therefore predictable, and the overall error can be overcome by mathematical modeling so that PtCO$_2$ allow a precise estimation of PaCO$_2$ and of PaCO$_2$ derived data such as $V_D/V_T$.

In brief our model allows to accurately estimate PaCO$_2$ from PtCO$_2$ during a maximal effort exercise and notably it allows to analyze exercise induced PaCO$_2$ changes.

In terms of mathematical method, the presented article implemented a correction based on multiple regression. The implemented correction was performed by minimizing the error with a fitting on the existing samples, but if piecewise linearity is assumed the correction remains valid at any time sample between the beginning of the loaded pedaling of the ramp protocol and 10 min afterwards. The validity of the applied correction is therefore limited to this 10 min ramp protocol.

This correction method can be further improved by acquiring more data samples with the same technique and retraining the regression model accordingly. Another strategy could be in changing the timestamps for some subjects, for instance in sampling after 1, 3, 5, 7 and 9 min, to make the model more robust. Models that consider the correlated nature of such measurements could be also exploited, such as mixed-effects models. With an increasing number of subjects, however, it will be possible to use artificial intelligence techniques, such as strategies based on machine learning [33] and deep learning. In terms of time series forecasting, deep learning techniques are highly performing [34] and continuously improving; examples of possible methods include convolutional neural networks (CNNs), multilayer perceptions (MLPs) and long-short term memory (LSTM) networks. Accordingly, the present results, this study can be considered as a preliminary and feasibility analysis.

The electrochemical sensor we tested for PtCO$_2$ measurements needs heating of the earlobe skin up to a temperature of 42 °C. Consequently, it can only be applied for a relatively short time and not to prolonged measurements. No safety issue related to heating arose during the study protocol. However, in the literature, other strategies have been studied to measure transcutaneous blood gases and overcome the limitations of electrochemical sensors. As regards CO$_2$ there have been recent projects attempting to measure PtCO$_2$ with optical sensors, with a technology which is conceptually similar to pulse oximetry. These attempts include using an optical CO$_2$ NDIR (non-dispersive infrared) sensor. Since CO$_2$ gas reacts to 4.3 µm wavelength, this wavelength is selected using an optical filter before the sensor, so that only the presence of CO$_2$ is detected [35]. With this technique, it might become possible to have more responsive sensors compared to electrochemical ones, thus better performances in continuous measurements with changes in parameters. This type of sensors could also be embedded in wearable devices, as it has been recently published by Tipparaju et al. [36], or garments [37] and integrated in telemedicine platforms [38], thus overcoming the limitations of measurements that are obtained in laboratory settings under the supervision of the clinician. Finally, optical sensors do not require any change of membrane, thus reducing the costs and making it possible to obtain also unsupervised measurements [7,20].

The present findings are a relevant step forward toward an extension in clinical practice of integrated exercise analysis which is needed for a better comprehension of exercise abnormalities [22]. Indeed, it allows to know PaCO$_2$ dynamics during exercise without an arterial catheter otherwise needed for multiple sampling. At present, in the clinical field,
direct or ear lobe PaCO$_2$ are omitted or measured only immediately after the end of exercise limiting the observation of data only to peak exercise. Vice versa, PtCO$_2$ continuous analysis allows to reliably estimate PaCO$_2$ changes during exercise and precisely to obtain data at the anaerobic threshold, during the isocapnic buffering period as well as at the respiratory compensation point also known as the second ventilatory threshold. Indeed, PaCO$_2$ data collected at these exercise steps provide relevant information about the chemoreflex regulation of ventilation and the causes of exercise induced hyperventilation which can be associated to V$_D$/V$_T$ as well as to reflex regulation [39]. As regards heart failure the information obtainable by PtCO$_2$, and therefore PaCO$_2$, V$_D$/V$_T$ and ∆PetCO$_2$-PaCO$_2$ allow to evaluate the possible presence of a concomitant lung disease, the reflex regulation of ventilation as well as the development during exercise of ventilation perfusion mismatch in the lung [6]. Moreover, the knowledge of PaCO$_2$ values and derived data during exercise will allow a more personalized and efficacious heart failure therapy for examples as regards the choice of the of the most efficacious β-blocker in a specific patient [40].

Moreover, PtCO$_2$ analysis seems to us a promising technique for future studies providing continuous information on CO$_2$ changes and therefore to assess, much better than with repeated arterial blood sampling, CO$_2$ dynamics, ventilation/perfusion mismatch, blood flow, through alveolar to earlobe transit time, and chemoreflex, through the CO$_2$ value during the isocapnic buffering period.

However, at present, a few limitations to the widespread use of the present technique must be acknowledge, such as the cost of the instrumentation, the time needed to heat the system before its use and the need of studies about its reliability and reproducibility in larger populations of patients with different heart failure etiologies and severity, as well as in patients with different diseases. Finally, our modeling has been built in ramp exercise protocol with expected exercise duration of approximately 10 min. We do not know whether it works in longer or shorter exercise or with different exercise protocols. A personalized exercise protocol with a progressively increasing workload built to achieve peak exercise in 10 min is considered the more physiologically correct and should be chosen in most cases [21,41]. Of note our model cannot be applied to other transcutaneous PCO$_2$ transducers. To assess whether this method has clinical applicability, an external validation is required, such as a replication in a greater, different cohort. Furthermore, we studied a mainly male HF population. Accordingly, our results should be applied with caution in female patients at least before a dedicated study is done on female HF patients. Finally, as PtCO$_2$ is largely affected by age, skin thickness, local temperature, usage of vasoactive drugs, poor tissue perfusion, and acidosis, the correlation between PtCO$_2$ and PaCO$_2$ might vary when these conditions exist: for this reason, our results should be applied only during exercise and in HF patients.

5. Conclusions

In heart failure patients PtCO$_2$ is a reliable PaCO$_2$ estimation at rest and at low exercise intensity. At high exercise intensity the overall response appears delayed but reproducible and the error can be overcome by mathematical modeling. In conclusion, during exercise PaCO$_2$ and V$_D$/V$_T$ can be estimated from PtCO$_2$ at rest and during a maximal workload exercise provided that a correction of a time delay is applied. A widespread use of this technique will likely enhance our knowledge in exercise physiology and allow a more personalized and efficacious patients assessment and, hopefully, treatment.

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