Passive temperature control based on a phase change metasurface

Sheng-Rui Wu, Kuan-Lin Lai & Chih-Ming Wang

In this paper, a tunable mid-infrared metasurface based on VO₂ phase change material is proposed for temperature control. The proposed structure consisting of a VO₂/SiO₂/VO₂ cavity supports a thermally switchable Fabry-Perot-like resonance mode at the transparency window of the atmosphere. Theoretically, the radiative cooling power density of the proposed metasurface can be switched to four-fold as the device temperature is below/above the phase change temperature of VO₂. Besides radiative cooling, a passive temperature control application based on this huge cooling power switching ability is theoretically demonstrated. We believe the proposed device can be applied for small radiative cooling and temperature control applications.

Plasmonic metamaterials and metasurfaces have been demonstrated for their ability to manipulate almost the entire range of properties of incident electromagnetic waves, for example, manipulating the amplitude, polarization, propagation direction, frequency and phase and so on. A lot of corresponding applications have been proposed based on the metamaterials and metasurfaces. Recently, manipulating thermal emission by using plasmonic metamaterials has received great attention and various applications are thus proposed. A series of works shows that the thermal emission from plasmonic metamaterial can be modified according to the geometric parameters of the structure. As the emission wavelength is tuned to be at the transparency window of the atmosphere, cooling effects based radiation can be achieved. In 1977, Bartoli et al. first demonstrated passive radiative cooling at night. Daytime radiative cooling is more challenging compared to nighttime radiative cooling, however, owing to the solar heating. In 2014, Raman et al. first successfully demonstrated daytime passive cooling. In that study, a 5 °C reduction below the ambient temperature under direct sunlight was experimentally demonstrated. Since then, radiative cooling, i.e. radiating heat to the cold sink of outer space via the transparency window of the atmosphere, has received a lot of research interest. Additional energy and resources to carry heat away are not needed during the radiative cooling process. Alongside these experiments, a lot of theoretical works aimed at designing various photonic and plasmonic structures for radiative cooling applications have also been proposed. In particular, low-cost radiative cooling without external active devices is of much interest.

By combining phase change material and metamaterial, a tunable/reconfigurable metamaterial can be realized. For example, the focused features of a germanium-antimony-tellurium (GST) alloy metalens can be optically controlled and switched. The resonant frequency of a metamaterial can be thermally tuned based on VO₂ phase transition. This means one can not only tune the emission peak at the transparency window of the atmosphere by tuning the geometric parameters of the metamaterial but also by tuning the temperature of a phase change material. Besides of reconfigurable metamaterials, VO₂ has been demonstrated in various applications such as thermal diodes, thermal transistors, thermal memories and thermochromic smart coating.

In this paper, we propose a SiO₂/VO₂ multilayer metasurface for a radiative cooling device. The SiO₂/VO₂ multilayer forms a thermally tunable metal/insulator/metal (MIM) cavity. The absorption spectrum of the designed structure shows the absorption at the transparency window of the atmosphere regime dramatically changed as the insulator phase VO₂ phase changes to be a metal phase one. We believe the proposed structure can be used as a tunable radiative cooling and passive temperature control device.

Schematic of the Phase Change Metasurface

The schematic of the investigated phase change metasurface is shown in Fig. 1. The structure consists of a silicon substrate, SiO₂ film, VO₂ film, SiO₂ wire and VO₂ wire, from bottom to top. The thickness of the SiO₂ film and VO₂ film is denoted by T_{SiO₂} and T_{VO₂}, respectively. The thickness of the SiO₂ wire and VO₂ wire is denoted by W_{SiO₂} and W_{VO₂}, respectively. The width of the SiO₂ wire and VO₂ wire are identical and denoted by W. The incident angle is denoted by θ_{inc}. The periodicity of the structure is denoted by Λ. Here, Λ is fixed to be 3 μm. This

Department of Opto-electronic Engineering, National Dong Hwa University, Hualien, 97401, Taiwan.
Correspondence and requests for materials should be addressed to C.-M.W. (email: wangcm@gms.ndhu.edu.tw)
structure can be fabricated by sequentially coating SiO\textsubscript{2}/VO\textsubscript{2}/SiO\textsubscript{2}/VO\textsubscript{2} film onto a silicon substrate. Then, the SiO\textsubscript{2} wire and VO\textsubscript{2} wire can be made by etching the top SiO\textsubscript{2}/VO\textsubscript{2} film using a one-step focused ion beam (FIB).

The optical properties of the phase change metasurface are simulated using the rigorous coupled-wave analysis (RCWA) method. The complex dielectric constants of SiO\textsubscript{2} are taken from ref.\textsuperscript{18}. The complex optical constants of the monoclinic insulator phase and rutile metal phase of VO\textsubscript{2} phase change material are taken from ref.\textsuperscript{19}. Although the phase change temperature of VO\textsubscript{2} might be slightly changed due to the difference in microstructure and crystallinity at different nucleation conditions resulting from various fabrication processes, the most common phase change temperature is 68 °C. It has also been shown that the transition temperature of the insulator-to-metal transition of VO\textsubscript{2} is narrower than 1 °C\textsuperscript{20}. Therefore, we can simply assume that the VO\textsubscript{2} is in metal-phase as the device temperature $T_{\text{dev}} > 68 \degree$C while it is in insulator-phase as $T_{\text{dev}} < 68 \degree$C.

### Spectral Response of Proposed Phase Change Metasurface

Figures 2a,b shows the absorption spectra of the VO\textsubscript{2} metasurfaces for a normally incident light. The incident light is TM-polarized (electric vector is perpendicular to the grating grooves). The TE-polarized light is also simulated. However, because of no significant resonance in the investigated spectral range, it is not shown here. Both the insulator-phase and metal-phase of VO\textsubscript{2} are simulated and shown in Fig. 2a and b, respectively.
the simulated geometric parameters of the VO₂ metasurfaces are $F_{\text{SiO}_2} = 100 \text{ nm}$, $F_{\text{VO}_2} = 100 \text{ nm}$, $T_{\text{SiO}_2} = 400 \text{ nm}$, $T_{\text{VO}_2} = 400 \text{ nm}$ and $\Lambda = 3000 \text{ nm}$. Black, red, and blue solid lines represent the metasurfaces with $W = 1.6 \mu\text{m}$, $W = 1.7 \mu\text{m}$ and $W = 1.8 \mu\text{m}$, respectively. For $\lambda = 8 \mu\text{m}$ to $13 \mu\text{m}$, it is referring to the transparency window of the atmosphere. For the insulator-phase of VO₂, the spectral response of the metasurface shows a clear absorption peak at $9.6 \mu\text{m}$ with an absorption of 0.6. This absorption is mainly contributed by the longitudinal optical (LO) vibration mode of SiO₂. Additionally, it has also reported that the LO/TO (transverse optical) vibration frequency of deposited SiO₂ depends on the film thickness. In our simulation, we cannot faithfully represent characteristics of the thickness-dependent vibration frequency. Owing to the fact that the absorption is mainly contributed by the inherent absorption of SiO₂, it is shown that the resonance wavelength is almost the same as $W$ increases from $1.6 \mu\text{m}$ to $1.8 \mu\text{m}$.

As the device temperature $T_{\text{dev}} > 68 ^\circ \text{C}$, it can be seen that the absorption of the metasurface dramatically increases. The absorption at $9.6 \mu\text{m}$ is 0.6, which is similar to that of the metasurface of the insulator-phase VO₂. We also find a resonance absorption peak at $10.5 \mu\text{m}$ for $W = 1.6 \mu\text{m}$. As $W$ is increasing, the resonance wavelength shows a redshift that is almost linearly with a slope of 1.5 wavelength/width.

From the localized field distribution at absorption peaks, we can observe an anti-node of standing wave resonance along the z-direction at the SiO₂ wire for the metasurface of the insulator-phase VO₂ as shown in Fig. 2c. The magnitude of standing wave is 1.8 fold compared to that of the incident field. In contrast, the $H_y$ field (y-component of the magnetic field) is localized at the VO₂/SiO₂/VO₂ cavity, as shown in Fig. 2d. The metallic phase of VO₂ forms a metal/insulator/metal cavity to support a magnetic resonance mode. From the mode pattern, we can recognize that the resonance mode is a fundamental Fabry-Perot mode. The magnetic field oscillates along the x-axis. Consequently, a wild W corresponds to a longer resonance cavity that leads to a redshift of resonance as already shown in Fig. 2(b). This magnetic resonance mode prolongs the absorption path of the SiO₂. As a result, the SiO₂ absorption corresponds to the TO vibration around $10 \mu\text{m}$ and bond-bending vibration around $11 \mu\text{m}$ to $13 \mu\text{m}$ can be enhanced. The absorption enhancement can be switched off as the device temperature is below the phase change temperature of VO₂.

**Radiative Cooling Based on VO₂ Metasurface**

Here, we assume that the heat transfer is based on thermal radiation only. The heat transfer via convection and conduction is ignored. The heat radiates outside atmospheric transparency window and parasitically absorbs heat radiation from the atmosphere. Under this assumption, the net cooling power density, $P_{\text{net}}$, is given by:

$$P_{\text{net}} = P_{\text{dev}} - P_{\text{amb}}$$

where $P_{\text{dev}}$ and $P_{\text{amb}}$ denote the radiation power density of the device and the ambient atmosphere, respectively. $P_{\text{dev}}$ is designable through modifying the emissivity of the device.

$$P_{\text{dev}} = \int_0^{\pi/2} \int_0^\infty U_\lambda(T_{\text{dev}}, \lambda) \varepsilon_{\text{dev}}(T_{\text{dev}}, \lambda, \theta) d\lambda d\theta$$

where $U_\lambda$ is the spectral radiance of a blackbody which can be calculated from the Planck’s law. $\varepsilon_{\text{dev}}$ is the emissivity of the cooling device. According to Kirchhoff’s law of thermal radiation, the absorptivity is equal to the emissivity. The angle-dependent emissivity of the device can be obtained by simulating the angle-dependent absorption using RCWA.

The net cooling power density of the phase change metasurface as a function of the device temperature ($T_{\text{dev}}$) is shown as the black solid line in Fig. 3. The ambient temperature is assumed to be $27 ^\circ \text{C}$. The emissivity...
of the metasurface as a function of wavelength and observation angle is simulated using RCWA for both TE and TM-polarization. The geometric parameters of the VO₂ metasurface are: W = 1800 nm, ΛSiO₂ = 100 nm, FVO₂ = 100 nm, TSiO₂ = 400 nm, TVO₂ = 400 nm and Λ = 3000 nm. As previously mentioned, we assume that the heat transfer is based on thermal radiation only. The emissivity of the atmosphere is taken from ref. 22. For comparison, the net cooling power of both a bulk silicon and a silicon substrate coated with 300 nm VO₂ film are calculated and shown as pink and blue solid line in Fig. 3, respectively. As shown in Fig. 3, the net cooling power slightly increases as the device temperature is below the phase change temperature of VO₂. Once the device temperature is above the phase change temperature of VO₂ the cooling power of the metasurface dramatically increases. Before and after VO₂ phase change, the cooling power is 118 W/m² W/m² and 528 W/m², as Tdev = 67 °C and Tdev = 69 °C, respectively. As a comparison, the net cooling power of silicon substrate coated with 300 nm VO₂ film is 1.3 W/m² and 187 W/m² as Tdev = 67 °C and Tdev = 69 °C, respectively.

**Passive Temperature Control Based on VO₂ Metasurface.** Besides the radiative cooling effect, in this section, we will demonstrate how the proposed structure can be utilized as a passive temperature controller. Now, we assume that the metasurface is bonded on a heat source, for example, an electronic chip. At this time, net cooling power density becomes:

$$P'_\text{net} = P_{\text{dev}} - P_{\text{amb}} - P_{\text{sou}}$$

where $P_{\text{sou}}$ is the heat being transported to metasurface via heat conduction from a heat source. From the size of the metasurface and the specific heat capacity of SiO₂ and VO₂, we can simply calculate the required amount of heat needed to raise the temperature by ΔT Kelvin. Assuming an initial temperature, $T_{\text{ini}}$, $P_{\text{dev}}(T_{\text{ini}}, \lambda, \theta)$ can be obtained via Eq. (2). Assuming a small derivative time interval Δt, we are able to calculate the device temperature of the metasurface after Δt, i.e. $T_{\text{dev}}(0 + \Delta t)$ where $T_{\text{dev}}(t = 0) = T_{\text{ini}}$. Then, $P_{\text{dev}}(T_{\text{dev}}, \lambda, \theta)$ can be obtained. Iteratively calculating $T_{\text{dev}}(m \Delta t)$ for $m = 1, 2, 3, \ldots$, until $T_{\text{dev}}(m \Delta t) = T_{\text{dev}}((m-1) \Delta t)$ approaches zero, $T_{\text{dev}}$ as a function of time can be thus obtained.

First, we consider the case for $T_{\text{ini}} = 75^\circ C$. Note that the $P_{\text{net}}$ for just above and just below phase change temperature is 118 W/m² and 528 W/m², respectively. The $T_{\text{dev}}$ as a function of time is shown in Fig. 4. For the red solid line, we assume $P_{\text{sou}} = 528 W/m²$, at this time, $P_{\text{net}} < 0$ at 68 °C, where 68 °C indicates the temperature is just above phase change temperature. Therefore, the final temperature cannot converge to a specific temperature. For the blue solid line, we assume $P_{\text{sou}} = 400 W/m²$, at this time, $P_{\text{net}} > 0$ at 68 °C and $P_{\text{net}} < 0$ at 68 °C where 68 °C indicates the temperature is just below phase change temperature. Therefore, once $T_{\text{dev}} > 68^\circ C$, the device produces a radiative cooling effect. In contrast, once $T_{\text{dev}} < 68^\circ C$, the device produces a heating effect. As a result, $T_{\text{dev}}$ finally converges to 68 °C. Similarly, as we assume the $T_{\text{ini}} = 15^\circ C$ and $P_{\text{sou}} = 400 W/m²$, the device produces a heating effect, and the final temperature converges to 68 °C as well. As long as 118 W/m² < $P_{\text{sou}}$ < 528 W/m², the device temperature can converge to the phase change temperature of VO₂.

Finally, we demonstrate that the $T_{\text{ini}}$ changes from 15 °C to 100 °C which is the common operation temperature of electronic chips. The $T_{\text{sou}}$ is assumed to be 400 W/m², which is also a common heat density generated from electronic chips. Figure 5 shows the device temperature as a function of Tini and time. It is shown that the final temperature can eventually converge to the corresponding phase change temperature. We, therefore, believe this passive temperature controller might be useful for maintaining the operation temperature of electronic devices. Although the control temperature can only be the phase change temperature of the utilized phase change material, it has been demonstrated that the phase change temperature of VO₂ can be modified by doping. For example, the phase change temperature can be decreased by doping W into VO₂ by 23 °C/wt%². Alternatively, doping Mg or Mo can also significantly decrease the phase change temperature. Consequently, we believe the controlled target temperature of the proposed passive temperature control metasurface can be modified by doping VO₂.
Conclusion

In summary, a mid-IR tunable metasurface consisting of a VO$_2$ and SiO$_2$ multilayer structure is proposed. It is shown that a FP-like fundamental mode at the transparency window of the atmosphere in VO$_2$/SiO$_2$/VO$_2$ cavity can be thermally switched. The absorption spectrum of the proposed phase change metasurface can be dramatically changed at the transparent window as the device temperature goes below/above the phase change temperature of VO$_2$. Theoretically, the radiative cooling power of the proposed metasurface can be thermally switched up to four-fold. Based on this huge cooling power switching ability, a passive temperature control application is theoretically demonstrated. We believe the proposed device can be applied for small radiative cooling and temperature control applications.

Methods

The optical properties of the phase change metasurface are simulated using the RCWA method. It is a semi-analytical method for solving the transmission, reflection, diffraction and field profiles of a periodic structure. The structures and fields are decomposed as a sum of spatial harmonics during the simulation. Here, we use 23 harmonics to obtain convergent results due to the localized nature of the plasmonic resonances.

References

1. Hsiao, H. H., Chu, C. H. & Tsai, D. P. Fundamentals and Applications of Metasurfaces. Small Methods 1, 1600064 (2017).
2. Tsai, W. Y., et al. Material-assisted metamaterial: a new dimension to create functional metamaterial. Sci. Rep. 7, 42076 (2017).
3. Wang, C.-M. & Tsai, D. P. Lambertian thermal emitter based on plasmonic enhanced absorption. Opt. Express 24, 18382–7 (2016).
4. Liao, C. Y., et al. Quasi-coherent thermal radiation with multiple resonant plasmonic cavities. Appl. Phys. Lett. 109, 261101 (2016).
5. Costantini, D., et al. Plasmonic Metasurface for Directional and Frequency-Selective Thermal Emission. Phys. Rev. Applied 4, 014023 (2015).
6. Bartoli, B., et al. “Nocturnal and diurnal performances of selective radiators. Appl. Energy 3, 267–286 (1977).
7. Raman, A. P., et al. Mott Transition in VO$_2$ Revealed by Infrared Spectroscopy and Nano-Imaging. Phys. Rev. Lett. 112, 183901 (2014).
8. Rephaeli, E., et al. Quasi-coherent thermal radiation with multiple resonant plasmonic cavities. Appl. Phys. Lett. 109, 261101 (2016).
9. Rephaeli, E., Raman, A. & Fan, S. Ultrabroadband photonic structures to achieve high-performance daytime radiative cooling. Nano Lett. 13, 1457–1461 (2013).
10. Gentle, A. R. & Smith, G. B. Radiative heat pumping from the earth using surface phonon resonant nanoparticles. Nano Lett. 10, 373–379 (2010).
11. Hossain, M. M., et al. A metamaterial emitter for highly efficient radiative cooling. Adv. Opt. Mater. 3, 1047–1051 (2015).
12. Zhang, Q., et al. Scalable manufactured randomised glass-polymer hybrid metamaterial for daytime radiative cooling. Science 355, 1062–1066 (2017).
13. Wang, G., et al. Optical Reconfigurable Photonic Devices” Nat. Photon. 10, 60–65 (2016).
14. Dickson, M. J., et al. Frequency tunable near-infrared metamaterials based on VO$_2$ phase transition. Opt. Express. 17, 18330 (2009).
15. Otey, C. R., Wu, Y. & Fan, S. Thermal Rectification through Vacuum. Phys. Rev. Lett. 104, 154301 (2010).
16. Ben-Abullah, B. et al. Near-Field Thermal Transistor. Phys. Rev. Lett. 112, 044301 (2014).
17. Zhu, J., et al. Vanadium Dioxide Nanoparticle-based Thermochromic Smart Coating: High Luminous Transmittance, Excellent Solar Regulation Efficiency, and Near Room Temperature Phase Transition. ACS Appl. Mater. Interfaces 7, 27796–27803 (2015).
18. Palik, E. D. Handbook of Optical Constants of Solids. (Academic Press, San Diego, 1998).
19. Wang, H., et al. Switchable wavelength-selective and diffuse metamaterial absorber/emitter with a phase transition layer. Appl. Phys. Lett. 105, 071907 (2014).
20. Ozilbash, M. M., et al. Mott Transition in VO$_2$, Revealed by Infrared Spectroscopy and Nano-Imaging. Science 318, 1750 (2007).
21. Osisskovski, R. & Drevillon, B. Infrared ellipsometry study of the thickness-dependent vibration frequency shifts in silicon dioxide films. J. Opt. Soc. Am. A 12, 1797–1804 (1995).
22. IR Transmission Spectra, Gemini Observatory Kernel Description. http://www.gemini.edu/?q/node/10789, accessed Nov 20, 2016.
23. Jin, P. & Tanemura, S. Relationship between transition temperature and x in V$_1$xW$_{1-x}$O$_2$ films deposited by dual-target magnetron sputter. Jpn. J. Appl. Phys. 34, 2459–2460 (1995).
24. Greenberg, C. B. Optically switchable thin films: a review. Thin Solid Film 251, 81–93 (1994).

Figure 5. Metasurface temperature as a function of initial temperature and time for $P_{sou} = 400$ W/m$^2$. 
Acknowledgements
The authors are grateful for the financial support of this research received from the Ministry of Science and Technology, Taiwan (Grant Nos 104-2221-E-259-028-MY3).

Author Contributions
S.R. Wu, K.L. Lai, and Chih-Ming Wang performed the numerical computations. C.M. Wang proposed the concept and writing the manuscript.

Additional Information
Competing Interests: The authors declare no competing interests.

Publisher’s note: Springer Nature remains neutral with regard to jurisdictional claims in published maps and institutional affiliations.

Open Access This article is licensed under a Creative Commons Attribution 4.0 International License, which permits use, sharing, adaptation, distribution and reproduction in any medium or format, as long as you give appropriate credit to the original author(s) and the source, provide a link to the Creative Commons license, and indicate if changes were made. The images or other third party material in this article are included in the article’s Creative Commons license, unless indicated otherwise in a credit line to the material. If material is not included in the article’s Creative Commons license and your intended use is not permitted by statutory regulation or exceeds the permitted use, you will need to obtain permission directly from the copyright holder. To view a copy of this license, visit http://creativecommons.org/licenses/by/4.0/.

© The Author(s) 2018