Thermodynamic evidence for a nematic phase transition at the onset of the pseudogap in \( \text{YBa}_2\text{Cu}_3\text{O}_y \)

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A long-standing controversial issue in the quest to understand the superconductivity in cuprates is the nature of the enigmatic pseudogap region of the phase diagram\(^1\). Especially important is whether the pseudogap state is a distinct thermodynamic phase characterized by broken symmetries below the onset temperature \( T^* \). Here we report torque-magnetometry measurements of anisotropic susceptibility within the \( ab \) planes in orthorhombic \( \text{YBa}_2\text{Cu}_3\text{O}_x \) with exceptionally high precision. The in-plane anisotropy displays a significant increase with a distinct kink at the pseudogap onset temperature \( T^* \), showing a remarkable scaling behaviour with respect to \( T/T^* \) in a wide doping range. Our systematic analysis reveals that the rotational symmetry breaking sets in at \( T^* \) in the limit where the effect of orthorhombicity is eliminated. These results provide thermodynamic evidence that the pseudogap onset is associated with a second-order nematic phase transition, which differs from the recently reported charge-density-wave transition that accompanies translational symmetry breaking\(^8-10\).

The pseudogap state harbours anomalous electronic states such as Fermi arcs, charge density waves (CDW), and \( d \)-wave superconductivity\(^1\). Electronic nematicity, a four-fold (\( C_4 \)) rotational symmetry breaking, has emerged as a key feature inside the pseudogap regime\(^1,11-14\), but the presence or absence of a nematic phase transition and its relationship to the pseudogap remain unresolved. Nematicity has been widely discussed in cuprates, and one of its mechanisms is the onset of a stripe-type CDW order parameter which generally breaks rotation symmetry as well as translation symmetry with a nonzero wavenumber \( Q \neq 0 \) (refs 2–10,15–18). In \( \text{Bi}_2\text{Sr}_2\text{CaCu}_2\text{O}_8 \) (BSCCO), scanning tunnelling microscopy experiments at low temperatures report an electronic state, consisting of short-range CDW of unidirectional (one-dimensional, 1D) type with a period of \( \approx 4a_0 \), where \( a_0 \) is the \( Cu-O-Cu \) distance\(^11\). This nano-stripe structure persists even well above the superconducting transition temperature \( T_c \) (ref. 21). In \( \text{YBa}_2\text{Cu}_3\text{O}_y \) (YBCO), the short-range CDW order forms a dome-shaped boundary inside the pseudogap regime\(^15\). Resonant X-ray scattering (RXS) experiments in YBCO report that the CDW is of unidirectional type with a periodicity of \( \approx 3a_0 \) (ref. 4).

In both BSCCO and YBCO, the CDW forms domains with a size of \( \approx 3 \) nm in zero field, inside which the \( C_4 \) symmetry of the unit cell is strongly broken. In contrast to such CDW orders, the nematicity may also be caused by an instability without breaking translational symmetry, characterized by \( Q = 0 \).

The measurement of the magnetic torque has a very high sensitivity for detecting magnetic anisotropy. The torque \( \tau = \mu_0 V \text{M} \times \text{H} \) is a thermodynamic quantity, a differential of the free energy with respect to angular displacement. Here \( \mu_0 \) is the permeability of vacuum, \( V \) is the sample volume, and \( \text{M} \) is the magnetization induced by the external magnetic field \( \text{H} \). When \( \text{H} \) is rotated within the \( ab \) plane, \( \tau \) is a periodic function of double the azimuthal angle \( \phi \) measured from the \( a \) axis (Fig. 1a):

\[
\tau_{ab} = \frac{1}{2} \mu_0 H^2 [ (\chi_{aa} - \chi_{bb}) \sin 2\phi - 2\chi_{ab} \cos 2\phi ]
\]

where the susceptibility tensor \( \chi_{ij} \) is given by \( M_i = \Sigma_j \chi_{ij} H_j \). In a system with tetragonal symmetry, \( \tau_{ab} \) should be zero. When \( C_4 \) symmetry is broken, a nonzero \( \tau_{ab} \) appears as a result of \( \chi_{aa} \neq \chi_{bb} \) and/or \( \chi_{ab} \neq 0 \), depending on the orthorhombicity direction.

Figure 1b displays typical curves of magnetic torque measured as a function of \( \phi \). All the curves are perfectly sinusoidal, but deviation occurs only near \( T_c \) due to diamagnetic susceptibility originating from superconducting fluctuations (see Methods and Supplementary Information). In the temperature range shown here, the oscillations are proportional to \( \sin 2\phi \) with a positive sign, indicating \( \chi_{aa} > \chi_{bb} \) and \( \chi_{ab} = 0 \) (Fig. 1c). Figure 2a–c depicts the amplitude of the in-plane anisotropy of the susceptibility, \( \Delta \chi_{ij} \equiv \chi_{aa} - \chi_{bb} \), at \( \mu_0 H = 7 \text{T} \) for underdoped YBCO with \( T_c = 60, 70 \) and 90 K (hole concentration \( p \approx 0.11, 0.13 \), and 0.15), respectively. In all the crystals, as the temperature is lowered, \( \Delta \chi_{ij} \) gradually decreases, then increases rapidly after exhibiting a distinct kink at \( T = T_c \). Since the average of uniform susceptibilities \( \chi_{aa} \) and \( \chi_{bb} \) is also temperature dependent, we introduce a dimensionless order parameter \( \eta \equiv (\chi_{aa} - \chi_{bb})/(\chi_{aa} + \chi_{bb}) \), a diagonal component of a nematic traceless symmetric tensor in two spatial dimensions, to discuss the nematicity properly (see Fig. 2d–f, and Methods). Above \( T_c \), \( \eta(T) \) is nearly independent of temperature, indicating that the uniform susceptibility causes a weak temperature dependence of \( \Delta \chi_{ij} \) above \( T_c \). Below \( T_c \), \( \eta(T) \) increases with a slightly concave curvature.

Figure 3 displays the temperature–doping phase diagram of YBCO. Obviously \( T_c \) coincides well with the pseudogap temperature \( T^* \) determined by various other probes. In what follows, we identify \( T_c \) as the pseudogap onset temperature \( T^* \) (that is, \( T_c = T^* \)). The kink anomaly in the temperature dependence of \( \Delta \chi_{ij} \) is usually an indication of a second-order phase transition. However, the \( C_4 \) symmetry is already broken due to the orthorhombic crystal structure with 1D CuO chains in YBCO, and thus no further
rotational symmetry breaking is expected. Indeed, \( \eta(T) \) is finite even above \( T^\ast \) for all the samples (Fig. 2d–f), confirming that the orthorhombic structure generally leads to anisotropic magnetic susceptibility. We note that the magnitude of \( \eta(T^\ast) \) increases with hole doping, which may be explained by the increased crystal orthorhombicity through the oxidation of CuO chains with doping.

Disentangling the intrinsic electronic nematicity in the CuO planes from extrinsic effects due to crystal orthorhombicity has been a vexing issue, particularly in YBCO. It should be stressed that the doping dependence of \( \eta(T^\ast) \) is a vexing issue, particularly in YBCO. It should be stressed that the doping dependence of \( \eta(T^\ast) \) is a vexing issue, particularly in YBCO. It should be stressed that the doping dependence of \( \eta(T^\ast) \) is a vexing issue, particularly in YBCO. It should be stressed that the doping dependence of \( \eta(T^\ast) \) is a vexing issue, particularly in YBCO. It should be stressed that the doping dependence of \( \eta(T^\ast) \) is a vexing issue, particularly in YBCO.

The second-order nematic phase transition at \( T^\ast \) is further supported by the scaling property of the nematicity for crystals with various hole concentrations. Although \( T^\ast \) and \( \eta(T^\ast) \) both have strong doping dependence, the excess anisotropy \( \Delta \eta(T) \) exhibits a good scaling behaviour when plotted as a function of \( T/T^\ast \). Figure 4b depicts \( \Delta \eta(T) \) normalized by the value at \( T = 0.7T^\ast \) versus \( T/T^\ast \). All the curves collapse into a single curve in a wide temperature range. Moreover, the data in the limit of no background anisotropy (Fig. 4a) lie on the same curve. It is well known that genuine second-order phase transitions do not occur in the presence of an external symmetry-breaking field and the kink-type temperature dependence of order parameters will be smeared out. However, if the external field is small enough, the kink behaviours are modified only slightly near the transition points, and scaling properties should prevail. In the present case, the crystal orthorhombicity in YBCO is the external symmetry-breaking field. At the same time, orthorhombic distortion would be helpful in preventing the formation of microscopic domains with orthogonal nematic directions, and thus important for the two-fold nematic signals to be observed in the bulk measurements.

The data collapse onto the universal curve in Fig. 4b indicates that the influence of the background anisotropy on the nematic order parameter is small except in the vicinity of \( T^\ast \). This supports that the crystal orthorhombicity is a small perturbation on the second-order transition and reinforces our analysis using background subtraction. The characteristic super-linear temperature dependence of \( \Delta \eta(T) \) appears at the onset of the nematicity. If one interprets the temperature dependence with the critical exponent \( \beta \), \( \Delta \eta(T) \propto (T^\ast - T)^\beta \), then the critical exponent shows large deviations from all known results of two-dimensional nematic transitions; for example, those of the mean-field \( (\beta = 1/2) \) and the 2D Ising model \( (\beta = 1/8) \). Although the super-linear dependence

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**Figure 1** In-plane torque magnetometry in YBCO single crystals. a. Schematic representation of the experimental configuration for torque measurements under an in-plane field rotation. An unwinned single-crystalline sample of YBCO is mounted on the piezo-resistive lever, which forms an electrical bridge circuit with the neighbouring reference lever. b. Typical curves of magnetic torque \( \tau \) in YBCO (\( p \approx 0.13 \)) as a function of the azimuthal angle \( \phi \) from the \( a \) axis. A field of \( \mu_0 H = 7 \text{T} \) is applied within the \( ab \) plane with a misalignment of less than \( 0.1^\circ \). c. Schematic view of the CuO\(_2\) plane. Because of the orthorhombic crystal structure stabilized by CuO chains (\( || b \) axis) lying between the CuO\(_2\) bilayers, \( \chi_{bb} > \chi_{ab} \).
may be due to some nontrivial temperature dependence of the nematic domain size, the unusual exponent may be associated with a novel transition in a very different universality class, which calls for further theoretical investigation, including scenarios of composite order parameters with randomness and doped spin liquids31,32.

Although the second-order phase transition at $T^*$ has been suggested by several experiments, it is far from settled. Resonant ultrasound spectroscopy experiments report a critical slowing down behaviour in the ultrasound absorption as $T^*$ is approached33, but a different interpretation without critical phenomena has been proposed34. The polarized neutron scattering experiments report time reversal symmetry breaking (TRS) with the appearance of a magnetic moment at $T^*$, which has been interpreted as circulating current loops within the CuO$_2$ unit cell35,36. However, polar Kerr effect measurements report that the TRS temperature is significantly different from $T^*$ (ref. 29). Enhancement of the in-plane anisotropy of the Nernst coefficient at $T^*$ has been reported37, but more recent results have shown that such an enhancement is much more pronounced below $T_{\text{CDW}}$ rather than $T^*$ (ref. 30). These results are in sharp contrast to our torque experiments, in which no discernible anomalies are observed at $T_{\text{CDW}}$. Recent RXX experiments report the appearance of orthogonal CDW domains with $Q_1 \approx (1/3,0,L)$ and $Q_2 \approx (0,1/3,L)$ (ref. 4). Our results suggest that the effective cancellation of the nematicity occurs due to nearly equal numbers of these CDW domains. We also point out that no anomaly in $\eta(T)$ is expected at $T_{\text{CDW}}$ when a background anisotropy due to the crystal orthorhombicity, $\eta(T_0)$, increases rapidly with $T$ (see also Methods).

Figure 2 | In-plane anisotropy of the magnetic susceptibility for underdoped YBCO with different hole doping levels. a-c. Temperature dependence of the in-plane anisotropy of the magnetic susceptibility, $\Delta \chi_i = \chi_{aa} - \chi_{bb}$, determined from the torque curves for underdoped YBCO with hole concentration $p \approx 0.11, 0.13$ and $0.15$, respectively. For all crystals, $\Delta \chi_i$ decreases gradually down to $T_r$ then increases rapidly below $T_r$ after exhibiting a kink at $T_r$. d–f. Temperature dependence of the order parameter $\eta = (\chi_{aa} - \chi_{bb})/(\chi_{aa} + \chi_{bb})$ for $p \approx 0.11, 0.13$ and $0.15$ (see Methods for detailed procedure to deduce $\eta$), respectively. Above $T_r$, $\eta(T)$ is independent of temperature, whereas it shows steep increases below $T_r$. In sharp contrast to the anomaly at $T_r$, no discernible anomaly is observed at the CDW transition temperature $T_{\text{CDW}}$. The background anisotropy due to the crystal orthorhombicity, $\eta(T_0)$, increases rapidly with $p$ (see also Methods).
Figure 3 | Temperature-doping phase diagram of YBCO. The phase diagram contains at least four different ordered phases, including antiferromagnetism (grey), superconductivity (yellow), CDW (pink) and pseudogap (blue) regimes. The pseudogap line (dashed line) at $T^*$ marks the boundary between the strange metal and even more anomalous regimes. Red circles represent the second-order nematic transition temperature $T_c$ determined by the present in-plane torque magnetometry. For comparison, the pseudogap temperature determined by other probes are also plotted. Purple circles, orange triangles and blue circles are $T^*$ reported by ultrasound spectroscopy, polarized neutron scattering, and Nernst coefficients, respectively. Magenta triangles represent the formation temperature of the short-range CDW, $T_{CDW}$, reported by resonant X-ray measurements. Green circles are the temperature below which the time reversal symmetry is broken, reported by the polar Kerr effect.

is, the extension of the pseudogap temperature to $T \to 0$ suggests a nematic QCP. The second-order nature of the phase transition line, in general, implies the presence of critical fluctuations near the transition line, and in an extended regime around the QCP one may expect significant quantum critical fluctuations. Hence it is tempting to consider that the nematic quantum fluctuations influence the superconductivity as well as the strange metallic behaviour in the normal state of cuprates.

Methods

Methods, including statements of data availability and any associated accession codes and references, are available in the online version of this paper.

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Author contributions

T.N., T.L., J.P and B.K. prepared the high-quality single-crystalline samples. Y.S., H.M. and S.K. performed the magnetic torque measurements. Y.S., H.M., E.-G.M. and Y.M. analysed the data. S.K., E.-G.M., Y.K., T.S., B.K. and Y.M. discussed and interpreted the results and prepared the manuscript.

Additional information

Supplementary information is available in the online version of the paper. Reprints and permissions information is available online at www.nature.com/reprints. Publisher’s note: Springer Nature remains neutral with regard to jurisdictional claims in published maps and institutional affiliations. Correspondence and requests for materials should be addressed to Y.M.

Competing financial interests

The authors declare no competing financial interests.
Methods

Materials. High-quality single crystals of YBCO were grown by the flux method. The oxygen concentration was controlled by annealing the crystals at high temperatures under an oxygen or a nitrogen atmosphere. The hole doping levels were determined from x-ray data. For p ≈ 0.11, 0.13 and 0.15, we used naturally untwinned single crystals which were carefully selected under a polarized microscope. The crystal of p = 0.10 was mechanically detwinned by heating under uniaxial stress. The superconducting transition temperature T_c was characterized by the magnetization measurements. The crystals exhibit sharp superconducting transitions, with the value of T_c determined as the midpoint at 58, 60, 70 and 90 K for p = 0.10, 0.11, 0.13 and 0.15, respectively. A first-order vortex-lattice melting transition, which can be seen only in clean and homogeneous single crystals, is clearly observed in the crystals prepared by the same method, indicating the high quality of our crystals. For each crystal, the directions of the a and b axes were determined by X-ray diffraction.

Torque magnetometry. Magnetic torque is measured by the piezo-resistive micro-cantilever technique, which is a very sensitive probe of magnetic anisotropy. In this method, an isotropic Curie contribution from impurity spins is cancelled out. Carefully selected single crystals with typical dimensions of 250 × 250 × 50 μm^3 are used in the torque measurements. The in-plane and out-of-plane anisotropies of the magnetic susceptibilities can be measured depending on the geometry of the sample, which is mounted on the lever (see Fig. 1a and Supplementary Fig. 1a).

Supplementary Fig. 1b demonstrates typical magnetic torque τ in underdoped YBCO (p ≈ 0.13) when a field H is rotated within a plane including the c axis (out-of-plane torque magnetometry). Here, θ is the polar angle from the c axis. We note that all of the single crystals used in the present study exhibit a purely paramagnetic response with negligibly small hysteresis components. The τ(θ) curves are perfectly sinusoidal, and are fitted well by

\[ \tau_{\text{R}}(\theta, T, H) = \frac{1}{2} \mu_0 H^2 V \Delta \chi_{\perp} \sin 2\theta \]

where V is the sample volume, \( \mu_0 \) is the permeability of vacuum and \( \Delta \chi_{\perp} = \chi_a - \chi_c \) is the difference between the c-axis and the in-plane susceptibilities, which yields τ periodic oscillations with respect to θ rotation.

From the amplitude of the τ(θ) curves, we obtain the temperature dependence of \( \Delta \chi_{\perp} \) in YBCO with the hole concentration p ≈ 0.11, 0.13 and 0.15 (Supplementary Fig. 2a,b and c, respectively). At high temperatures, the magnitude of \( \Delta \chi_{\perp} \) changes nearly linearly with temperature. Upon cooling, the data deviate downward from the linear temperature behaviour below T_c, which represents the pseudogap formation. This is because the decrease in the density of states results in a suppression of the c-axis susceptibility as previously reported, for example, in Bi_{2-x}Sr_{x}CaCu_2O_{8+δ} (refs 46,47). We note that T_c determined by the out-of-plane torque magnetometry coincides well with the kink temperature T_k in the in-plane torque magnetometry.

For the in-plane torque magnetometry, the magnetic field H was precisely applied in the plane of the sample with an error of less than 0.1°. As shown in Fig. 1c, the in-plane response of the magnetic torque exhibits two-fold oscillations with respect to the azimuthal angle φ. We note that the oscillations are dominated only by the two-fold component and the higher-order components due to nonlinear susceptibilities are negligibly small in the whole temperature range we measured. This is evident by the Fourier analysis of the torque oscillations, in which the raw torque curve τ(φ) is decomposed as τ = τ_{2φ} + τ_{4φ} + ... , where τ_{2φ} = \Lambda_{2φ} \sin 2(\phi - \phi_0) is a term with 2n-fold symmetry with n = 1,2,3, etc. In Supplementary Fig. 3, we plot the amplitudes of the two-, four-, six- and eight-fold oscillations for underdoped YBCO with p ≈ 0.13. The amplitudes of the nonlinear susceptibilities (n ≥ 2) are two to three orders of magnitude smaller than the two-fold term, which comes from the anisotropy of linear susceptibility.

In-plane anisotropy of susceptibility. As the average of in-plane susceptibilities \( \chi_{\perp} = (1/2)(\chi_a + \chi_c) \) is dependent on temperature, we introduce a dimensionless order parameter \( \eta = (\chi_c - \chi_a)/(\chi_a + \chi_c) \), a diagonal component of a nematic traceless symmetric tensor, to discuss the nematicity properly. Here we refer to the magnetic susceptibility data of the powder samples of YBCO to obtain the systematic doping dependence of the denominator. Fairly generally, the magnetic susceptibility of powder samples is given by \( \chi_{\perp} = (1/3)\chi_a + (1/3)\chi_c + (1/3)\chi_b \) when off-diagonal terms in the susceptibility tensor can be ignored. By combining this with \( \Delta \chi_{\perp} = \chi_a - \chi_c \) determined from the out-of-plane torque magnetometry and \( \Delta \chi_{\perp} \equiv \chi_a - \chi_c \) from the in-plane torque magnetometry, a systematic doping dependence of \( \chi_{\perp} \) and \( \chi_a \) is obtained. Supplementary Fig. 4 depicts the temperature dependence of \( \chi_{\perp} \) and \( \chi_a \) obtained for YBCO with different hole concentrations. For all the doping levels, \( \chi_{\perp} \) and \( \chi_a \) both decrease monotonically as the temperature is lowered. The overall magnitude of \( \chi_a \) is also enhanced with doping. It should be noted that the difference between \( \chi_{\perp} \) and \( \chi_a \) exhibits a systematic increase as the holes are doped. This difference actually corresponds to the results of the in-plane torque magnetometry as demonstrated in Fig. 2a–c. Whereas the anisotropy of the in-plane susceptibility \( \Delta \chi_{\perp} \) is dependent on temperature above T_k, when normalized to the form \( \eta \) it becomes independent of temperature within the error, indicating that the weak temperature dependence of \( \Delta \chi_{\perp} \) above T_k is caused by the uniform susceptibility.

In Supplementary Fig. 5a–d, the temperature dependence of \( \Delta \chi_{\perp} \) for four samples measured here (p ≈ 0.1, 0.11, 0.13 and 0.15) is shown over a full temperature range from T_k up to ≈ 290 K, which is limited by our experimental set-up using a variable temperature insert in our superconducting magnet. In the superconducting state below T_k, the torque curve shows hysteresis due to the pinning effect of vortices. In the normal state close to T_k, the effect of superconducting fluctuations can be seen, which distorts \( \eta \) from the sinusoidal curve of sin 2θ because of the in-plane anisotropy of the upper critical field. This is demonstrated in Supplementary Fig. 6 by the amplitude of higher-order oscillation A_{nφ}, which becomes significant below doping-dependent temperatures T_{nφ} (open symbols). Above T_{nφ} we have a systematic evolution of \( \Delta \chi_{\perp} \) with doping: at high temperatures above T_k the strongly doping-dependent background component shows a weak temperature dependence with a positive d\Delta \chi_{\perp}/dT, and the kink anomaly is only found at T_k, below which all the data show an increasing trend with decreasing temperature. We find no significant anomaly at the CDW transition temperatures.

Data availability. The data that support the plots within this paper and other findings of this study are available from the corresponding author upon reasonable request.

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