Showcasing research from Professor Tarancón’s laboratory, Catalonia Institute for Energy Research (IREC), Catalonia, Spain.

Operando probing of Li-insertion into LiMn$_2$O$_4$ cathodes by spectroscopic ellipsometry

The work presents a novel Operando Spectroscopic Ellipsometry tool for the characterization of battery materials combining high spatial resolution with multi-layer and time-resolved capabilities. A proof of concept is shown where the lithium content of a LiMn$_2$O$_4$ thin film is tracked along voltage sweeps and fast potential steps.

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A. Morata, V. Siller, F. Chiabrera, M. Nuñez, R. Trocoli, M. Stchakovsky$^b$ and A. Tarancón$^a, c$

A novel non-destructive methodology for operando observation of ion intercalation and the state of charge on battery electrodes is presented based on spectroscopic ellipsometry (SE). The potentiality of this technique for performing time-resolved measurements of (de-)lithiation processes on electrode materials has been demonstrated using thin film spinel LiMn$_2$O$_4$ as a cathode for Li-ion batteries. The chemical diffusivity of Li$^+$ ions in this material has been determined by the time evolution of the Li insertion into the film, and in the light of these results, it has been possible to relate the controversial pseudo-capacitive behavior observed in this material to the nanostructure of the layer. The results presented here establish a new way for operando characterization of battery materials and devices providing a powerful tool for the understanding of ion diffusion mechanisms in a collection of electrochemical devices.

Introduction

Batteries are currently a mainstream high energy storage technology ubiquitously adopted in diverse applications ranging from electronic devices to vehicles and domestic energy storage. These new energy demands foster continuous advances for improving devices by achieving higher capacity, faster charge–discharge capabilities and longer lifetime. Advanced concepts in batteries typically involve exploring novel materials and interfaces and the related electrochemical and diffusive processes taking place during the operation of the device. In particular, it is crucial to gain insights into dominant interface phenomena such as Li$^+$ insertion, formation of solid electrolyte interphases (SEIs)$^{1,2}$ or ion blocking grain boundaries.$^{3-8}$ However, the continuous evolution of interfaces during the operation of devices makes it difficult to obtain reliable information only from post-mortem analyses after multiple cycles. For this reason, a lot of effort has been dedicated in the last decade for developing novel techniques to obtain new insights into interface phenomena in operando and therefore, into their direct correlation with electrochemical performances.$^{9-13}$ Despite these efforts, some of the most powerful techniques, such as isotopic ion exchange methods,$^{14}$ in situ TEM$^{14}$ and the collection of synchrotron radiation based techniques,$^{10,11,14-20}$ are highly sophisticated limiting the straightforward access to essential information for developing highly performing batteries. In addition, a number of commonly available techniques have also been explored including X-ray diffraction,$^{21-23}$ atomic force microscopy (AFM)$^{5,24}$ Raman spectroscopy$^{25-27}$ and Fourier transform infrared (FTIR) spectroscopy$^{28,29}$ showing different advantages and limitations regarding spatial and time resolutions. On the other hand, despite the well-known capabilities of Spectroscopic Ellipsometry (SE) for the study of the properties of thin film systems (including multi-layered devices), the use of this affordable technique in the field of Li-i is very limited$^{30}$ and, to the best of the authors’ knowledge, it has never been implemented for real in operando measurements in the battery domain. SE measures the change in the polarization state of a light beam reflected in the sample and compares it to a model. In this way, relevant optical properties of the material such as the dielectric function ($\varepsilon$) can be obtained as a function of the wavelength.$^{31}$ This technique is typically used to determine the properties of thin films and also complex multilayer systems, being sensitive to parameters such as crystallinity, materials ratio in mixtures, roughness, structure of the interfaces, etc.

In this work, an optical non-destructive methodology based on SE is proposed for the first time to provide information on the (de-)lithiation phenomenon occurring in a model electrode such as LiMn$_2$O$_4$ operating as a cathode in a Li-ion battery. Spinel LiMn$_2$O$_4$ is a low cost/low toxicity compound based on abundant raw materials showing high working potential and safety together with a competitive theoretical capacity (148 mA h g$^{-1}$).$^{32,33}$ Furthermore, this material has shown an...
outstandingly fast performance when presented in the nanostructured form, the origin of which is still a matter of controversy.\textsuperscript{34-41} This feature has important practical implications as it would allow development of devices that can simultaneously provide high power typical of capacitors, and high storage capacity expected from batteries.\textsuperscript{42} Due to the fast response of the SE system and the strong effect of the oxidation state on the optical properties of compounds, SE has been used in this work to monitor Li\textsuperscript{+} transport properties by real-time tracking of the valence changes associated with lithium insertion–deinsertion along LiMn\textsubscript{2}O\textsubscript{4} thin films and interfaces. Furthermore, SE is used to accurately measure the thickness and porosity of the films giving rise to values of effective diffusion of Li cations in LiMn\textsubscript{2}O\textsubscript{4}.

Results and discussion

LiMn\textsubscript{2}O\textsubscript{4} thin films were grown by pulsed laser deposition (PLD) on 80 nm-thick sputtered Pt layers deposited on top of 10 × 10 mm Si chips. A multilayer approach has been used to compensate the Li loss typically occurring in PLD deposition of lithium compounds to obtain the stoichiometric spinel phase (details on this procedure can be found elsewhere\textsuperscript{43,44}). Structural and morphological characterization of the multilayer structure and the LMO thin film has been carried out by SEM and AFM and the results are presented in Fig. 1. The SEM images show relatively large crystalline domains and a thickness of 330 ± 10 nm for the LMO layer. According to X-ray diffraction measurements presented in Fig. S1† the layer shows the appropriate spinel phase without secondary phases.

The as-prepared samples have been brought into contact with Al foil protected with a Kapton\textsuperscript{®} film and introduced in a homemade electrochemical measurement chamber, provided with optical windows and filled with a 0.2 M Li\textsubscript{2}SO\textsubscript{4} liquid electrolyte (a detailed description of the setup can be found in the Experimental section and elsewhere\textsuperscript{42}). Cyclic voltammetry (CV) measurements have been conducted, showing very well defined (de)lithiation double peaks typical of the spinel structure (see Fig. 2a). The results are consistent with profiles previously reported for analogous samples, which demonstrates high capacity retention and outstandingly fast performance typically attributed to the so-called pseudocapacitive phenomenon.\textsuperscript{42} Simultaneous with the electrochemical characterization, spectroscopic ellipsometry measurements have been carried out between \( U = 0.350 \) and 1.05 V, corresponding to completely lithiated and de-lithiated states, respectively (Fig. 2b). The important variations observed in the spectra are mainly due to the change in the Mn oxidation state in LMO, from Mn\textsuperscript{4+} to Mn\textsuperscript{3+}, occurring during the Li\textsuperscript{+} extraction. The significant change observed in the spectra indicates the high sensitivity of SE in monitoring the Li\textsuperscript{+} insertion/deinsertion process. In order to describe the sample in any oxidation state within the proposed voltage range, simple but flexible geometrical and physical models have been defined. The geometrical model consists of a dense film on top of a flat and completely opaque Pt substrate (see the sketch in ESI S2† and the inset in Fig. 2c). The porosity of the film has been modelled by using a partially empty top layer filled with the liquid electrolyte present in the electrochemical cell, whose optical properties have been measured using a prisma setup (as detailed elsewhere\textsuperscript{45}). On the other
hand, the physical model uses Tauc-Lorentz parameterization of the optical constants of the LiMn$_2$O$_4$ with four oscillators. A four-component configuration is the simplest model found that is able to track all the changes of the film during cycling. Previous knowledge on the spinel LiMn$_2$O$_4$ and MnO$_2$ band structures (i.e. the material in lithiated and delithiated states) has simplified the selection of the initial optical parameters giving them a clear physical meaning. In particular, the footprint for following the Li$^+$ insertion/deinsertion phenomena is expected to be linked to the adsorption bands at 2.8–3 eV and 3.4–3.6 eV, corresponding to the electronic transition from O$^2-$ (2p) to Mn$^{3+}$($e_g$) and Mn$^{4+}$($e_g$), respectively (see details on the oscillator model and fitting procedure in the Experimental section and ESI†). The experimental data and the fitting of the proposed model are in great agreement with the range of applied voltages of $U = 0.350–1.05$ V, therefore allowing the calculation of the evolution of the optical constants of LMO during cycling of batteries (Fig. 2b and S2c†).

Fig. 2b and c show the evolution of the SE spectra with time and the calculated optical constant during the galvanostatic charging of the battery (only the imaginary part of the dielectric function, $e_i$, is represented for the sake of simplicity). The optical properties of the multilayer structure are not significantly evolving out of the insertion potentials, namely, $V = 0.75$ and 0.95 V, while, at these potentials, the light absorption around 3 eV is clearly enhanced. This undoubtedly indicates that the oxidation/reduction of the film is directly correlated with its optical properties, which is fully confirmed by the identical change of the dielectric constant and the charge accumulated in the film during the voltage sweep (essentially proportional to Li$^+$ extraction), see Fig. 2d. The coincidence of both magnitudes allows the direct quantification of the Li content of the electrode layer at any time and applied voltage, i.e. the state of charge of the battery, by simply integrating the absorption band at 2.8 eV of the dielectric constant as obtained by non-destructive SE.
Complementary to the battery capacity and state of charge analysis, relevant mass transport information such as diffusivity was obtained for LMO by SE through the analysis of the transients between different charge states. Using an innovative triggering strategy to reconstruct fast transient sign along battery cycling (see the Experimental section/ESI† for further details), sample rates as high as 10 Hz (1 sample every 100 ms) were possible for relatively rough and highly absorbing LiMn$_2$O$_4$ layers. However, it is important to notice that there is no fundamental limitation that prevents reduction in this rate above 100 Hz in a conventional setup, as long as better conditions are provided (the sampling frequency depends on the signal-to-noise ratio, which is governed by experimental features of the sample and the system such as absorbance or surface roughness and electrolyte absorption or optical windows, respectively) or even increase in this frequency using advanced multi-wavelength ellipsometers (able to acquire the whole spectra at a time).

An experiment to induce complete de-lithiation of the LiMn$_2$O$_4$ layer was carried out by applying a potentiostatic step (with voltage changing from 0.35 to 1.05 V vs. Ag/AgCl). The corresponding transient of the dielectric function calculated after SE measurements is shown in Fig. 3a. A sudden change in the dielectric function at the moment of applying the voltage step is clearly observed. This observation can be quantified by integrating the optical absorption band at 2.8 eV, which yields the amount of Li ions inserted into the layer at every single point of time (Fig. 3b). From the obtained curve, an ultrafast oxidation process of LMO is derived showing an insertion of more than 80% of the final charge in less than 2 seconds. This result is consistent with the fast electrochemical performance previously observed for the same thin film cathodes by our group$^{42-44}$ and for other similar cathodes in the literature.$^{34-41}$ It has been speculated that shorter diffusion paths$^{39,42}$ and/or intimate contact with the current collector$^4$ are behind the fast kinetics leading to pseudocapacitive behaviour.

Here we unequivocally demonstrate this fact, as the accumulated charge (represented by the green line in the plot of Fig. 3b) remarkably coincides with the variation of $\varepsilon_1$ at 2.8 eV, which indicates that all of the introduced charge is immediately invested in the electrochemical oxidation of the bulk LMO (Mn$^{3+}$ to Mn$^{4+}$) without the need for any additional surface accumulation capacitive phenomena.

To further corroborate this point and to quantify mass transport properties of this material, the Li insertion as a function of time obtained by SE has been adjusted to a classical diffusion model calculated by the finite element method (see the ESI† section for details on the procedure). A simple geometry consisting of a cylinder representing an average columnar grain of the film on top of a fully blocking substrate has been used. The obtained results are represented by a green line in Fig. 3b showing excellent agreement with the experimental data therefore confirming the diffusional origin of the observed phenomena. According to the fitting, a chemical diffusivity for Li$^+$ into LMO of $D_{chem}$ $\approx 3.5 \times 10^{-12}$ cm$^2$ s$^{-1}$ is obtained, which is comfortably positioned within the wide range of values found in the literature for this particular material (ranging from $10^{-12}$ to $10^{-10}$ cm$^2$ s$^{-1}$ when measured with CV, potentiostatic intermittent titration or impedance spectroscopy methods).$^{3,48-57}$ All in all, from the here presented results, it is demonstrated that apparently ultrafast Li$^+$ deinsertion, potentially attributed to the pseudo-capacitive effect, can indeed be explained by using a special microstructure, providing a high surface area for Li$^+$ interchange with the electrolyte, even considering a modest diffusivity value. This first example highlights the potential of spectroscopic ellipsometry as a unique technique to carry out fundamental and practical studies of materials for batteries and battery devices in operando even when ultrafast phenomena are taking place.

**Experimental**

The deposition of LMO thin films was carried out using a Large Area PLD5000 from PVD Products, Inc. equipped with a KrF excimer laser with 248 nm wavelength. Multilayer deposition was used to compensate the Li loss, using LiMn$_2$O$_4$ and Li$_2$O.

**Fig. 3** Transient analysis of the LMO during cycling: (a) variation of the $\varepsilon_1$ of the LMO thin film during a sudden potential step from 0.35 to 1.05 V vs. Ag/AgCl. (b) Evolution of optical absorption at 2.8 eV of the dielectric function during this volt.
targets purchased from Neyco, France. Details about this procedure have been published elsewhere. Films were deposited onto Si/TiN (10 nm)/Pt (80 nm). The substrates were subjected to a cleaning process before deposition consisting of a subsequent bath in acetone, isopropanol and deionized water. The PLD process was performed in an oxygen atmosphere at a pressure of 20 mTorr. The deposition temperature was 650 °C. A laser fluency of 650 mJ cm⁻² with a pulse frequency of 10 Hz was used. LiMn₂O₄ and Li₂O materials were deposited alternately in a pulse ratio of 2:1 until the desired thickness was reached. XRD measurements were carried out using Bruker-D8 Advance equipment with a Cu Kα radiation source and a Lynx Eye detector. SEM images were taken using a Zeiss Auriga. Spectroscopic ellipsometry measurements were recorded by using a phase modulation system (UVISEL equipped with a Horiba spectrometer) at wavelengths ranging from 260 to 2100 nm (4.77 to 0.59 eV). The ellipsometer beam angle of incidence was fixed at 70.0°, and the spot size was fixed at 2 mm². A homemade electrochemical chamber was fabricated with a Prusa i3 style 3D printer, using Acrilonitril Butadiene Styrene. The frame of the chip (having the Pt layer exposed) was brought into contact with Al tape. The whole sample is covered with insulating Kapton tape, except for an 8 mm² slide in the center, which will be the active region in contact with both the electrolyte and the ellipsometer light. The chamber has two optical windows perpendicular to the light beam, made of CaF₂ from Thorlabs, providing a transmission window from 18 nm to 8 μm. In order to demonstrate that the chamber does not interfere with the results, a reference sample consisting of a bilayer of thermal oxide (ca. 100 nm) and silicon nitride (300 nm) on a Si (100) chip is consecutively measured both inside and outside the chamber. The results are identical, showing differences of measured thicknesses below 1 nm. Moreover, a reference measurement is always taken on the sample under test out of the chamber before the operando experiments. These results are compared to the ones obtained inside the cell, discarding any unimportant discrepancy. The chamber is covered with a liquid electrolyte (0.2 M Li₂SO₄) at a level above the optical windows. Counter and reference electrodes are introduced (Pt mesh and Ag/AgCl, 3 M KCl, respectively).

The effect of nanoporosity on the lithiation mechanism of LiMn₂O₄ thin films was investigated by FEM analysis. The simulations were performed by using COMSOL Multiphysics using the Transport of Diluted Species module. Details about the procedure are presented in ESI† section 4.

Conclusions

Spectroscopic ellipsometry has been presented as a new powerful tool for conducting operando measurements of Li-ion battery materials and devices. In particular, the evolution of the optical properties of LiMn₂O₄ cathodes has been obtained during cycling in a liquid electrolyte electrochemical cell. On this basis, the optical absorption of the film has been directly correlated with the Li insertion/deinsertion in steady states of battery charge, enabling a novel non-destructive measurement of the remaining capacity. Furthermore, the technique has proved its suitability for tracking the Li⁺ incorporation into a LiMn₂O₄ film during a fast discharging transient of only two seconds. This transient behaviour has been quantitatively described by using a FEM simulation, which allowed the determination of the effective diffusion coefficient of Li⁺ cations in LiMn₂O₄, which was estimated to be $D_{\text{chem}} = 3.5 \times 10^{-12}$ cm² s⁻¹ at room temperature. Moreover, this analysis showed that the apparent pseudo-capacitive performance, previously reported for LiMn₂O₄, can be directly explained by the high surface area of the porous structure of the layer. To the best of the authors’ knowledge, this is the first time that the SE technique has been used for operando studies of battery materials, therefore opening a new avenue for understanding mass transport properties and critical interfacial phenomena occurring during battery operation. Moreover, the high spatial resolution, multi-layer combined analysis and time-resolved capabilities of the technique will definitely contribute new insights into materials and devices at the nanoscale level for improving current performances by interface engineering.

Conflicts of interest

There are no conflicts to declare.

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