$P_{cs}(4459)$ and other possible molecular states from $\Xi_c^{(*)} \bar{D}^{(*)}$ and $\Xi_c^\prime \bar{D}^{(*)}$ interactions

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Recently, the LHCb Collaboration reported a new structure $P_{cs}(4459)$ with a mass of 19 MeV below the $\Xi_c \bar{D}^*$ threshold. It may be a candidate of molecular state from the $\Xi_c \bar{D}^*$ interaction. In the current work, we perform a coupled-channel study of the $\Xi_c \bar{D}^*$, $\Xi_c^\prime \bar{D}^*$, $\Xi_c \bar{D}$, $\Xi_c^\prime \bar{D}$, and $\Xi_c \bar{D}$ interactions in the quasipotential Bethe-Salpeter equation approach. With the help of the heavy quark chiral effective Lagrangian, the potential is constructed by light meson exchanges. Two $\Xi_c \bar{D}^*$ molecular states are produced with spin parities $J^P = 1/2^-$ and $3/2^+$. The lower state with $3/2^+$ can be related to the observed $P_{cs}(4450)$ while two-peak structure cannot be excluded. Within the same model, other strange hidden-charm pentaquarks are also predicted. Two states with spin parities $1/2^-$ and $3/2^+$ are predicted near the $\Xi_c \bar{D}$, $\Xi_c \bar{D}$, and $\Xi_c \bar{D}$ thresholds, respectively. As two states near $\Xi_c \bar{D}$ threshold, two states are produced with $1/2^-$ and $3/2^+$ near the $\Xi_c^\prime \bar{D}$ threshold. The couplings of the molecular states to the considered channels are also discussed. The experimental research of those states are helpful to understand the origin and internal structure of the $P_{cs}$ and $P_t$ states.

I. INTRODUCTION

Recently, the LHCb Collaboration released their results about the $\Xi_b \rightarrow J/\psi K^- \Lambda$ decay, which indicates a new resonance structure named $P_{cs}(4459)$, which carries a mass of 4458.8 $\pm$ 2.9 $^{+4.1}_{-1.1}$ MeV and a width of 17.3 $\pm$ 6.5 $^{+3.0}_{-2.2}$ MeV [1]. Such structure is just 19 MeV below the $\Xi_c \bar{D}^*$ threshold and the width is relatively narrow. It follows a series of observations about the hidden-charm pentaquarks. In 2015, the LHCb Collaboration firstly reported two structures $P_c(4380)$ and $P_c(4450)$ in the $\Lambda_b \rightarrow J/\psi K^- p$ [2], which are close to the $\Sigma_c \bar{D}$ and $\Sigma_c \bar{D}$ thresholds, respectively. Such observation confirmed previous predictions about the hidden-charm pentaquarks [3–6]. Due to the closeness to the thresholds, these structures were soon interpreted as molecular states in the literature [7–12]. Other pictures, such as compact pentaquark [13–15] and anomalous triangle singularity [16], were also proposed to explain the observation. In 2019, the LHCb Collaboration updated their results. The upper $P_c(4450)$ was found to be a two-peak structure named as $P_c(4457)$ and $P_c(4440)$, and a new structure, $P_c(4312)$, was observed near the $\Sigma_c \bar{D}$ threshold [17]. The new result strongly supports the molecular state picture. If we include the $P_c(4380)$ state, which was not confirmed but also not excluded by new observation, the four states provide a wonderful spectrum of $S$-wave states from the $\Sigma_c \bar{D} - \Sigma_c^\prime \bar{D} - \Sigma_c \bar{D}$ interaction.

The observation of the hidden-charm pentaquarks inspires a large amount of theoretical studies about their internal structure [18–29]. The partners of the hidden-charm pentaquarks were also widely discussed in the literature [30–38]. Replacing one of the light quark by strange quark, one can naturally obtain a strange hidden charm pentaquark, which have been studied in the pioneer work [3] and some studies after the observation of $P_c$ states [39–47]. The observation of these partners is very helpful to understand the internal structure of the pentaquarks.

The recent observation of $P_{cs}(4459)$ favors the molecular state interpretations of the hidden-charm pentaquarks [48–51]. It can be taken as the strange partner of the $P_c(4450)$. According to its mass, it can be assigned as the candidate of a $\Xi_c \bar{D}^*$ state with spin parity $J^P = 1/2^-$ or $3/2^+$. Due to lack of the partial-wave treatment, the current experimental analysis did not provide the information about its spin parity. From the experience of study about the $P_c(4450)$, one can expect that there may be two structures in the $P_{cs}(4459)$. In Ref. [47], the author predicted two $\Xi_c \bar{D}^*$ states with $J^P = 1/2^-$ and $3/2^+$ which carry masses of 4456.9 $^{+3.0}_{-2.6}$ and 4463.0 $^{+2.8}_{-3.0}$ MeV, respectively. Different mass order of two $\Xi_c \bar{D}^*$ states was also suggested in the literature. In Ref. [49], the calculation yields masses of 4469 and 4453 – 4463 MeV for states with 1/2 and 3/2, respectively.

In our previous work, the hidden-charm pentaquarks were well explained as molecular states in the quasipotential Bethe-Salpeter equation (qBSE) approach [26, 27], which was extended to predict the hidden-bottom pentaquarks [38]. Such studies provide a good theoretical frame to study the strange hidden-charm pentaquark. Due to the heavy quark symmetry, the model has been constrained by experimentally observed hidden-charm pentaquarks. Hence, it is interesting to perform a calculation about the molecular states from the $\Xi_c^{(*)} \bar{D}^{(*)}$ interaction in the same frame. The strange hidden-charm pentaquarks are also possibly produced from the interactions of charmed baryon and strange anticharm meson. Compared with the couplings between channels in the $\Xi_c^{(*)} \bar{D}^{(*)}$ interactions where the pion exchange is possible, the couplings between two types of interactions though kaon exchange should be weaker. Hence, in the current work, we consider six channels in $\Xi_c^{(*)} \bar{D}^{(*)}$ interaction, which are related to the $P_{cs}(4459)$.

With the help of the heavy quark chiral effective Lagrangians, which was also adopted to reproduce the hidden-charm pentaquarks, the one-boson-exchange model will be adopted in the current work to construct the interaction kernel to calculate the scattering amplitude by solving the qBSE. The molecular states can be studied by searching for the poles of the complex energy plane. The coupled-channel effects will be also included explicitly to produce the widths
of the molecular states. The molecular state interpretation of the $P_{cs}(4459)$ will be discussed based on the results. More molecular states will be also predicted, which can be searched in the future experiment.

This article is organized as follows. After introduction, Section II shows the details of dynamics of the $\Xi^*_c D^*$, $\Xi'_c D^*$, $\Xi_c^0 D$, $\Xi_c^0 D^*$, $\Xi'_c D$, and $\Xi^*_c D$ interactions, including the relevant effective Lagrangians, reduction of potential kernel and a brief introduction of the qBSE. In Section III, the results with single-channel calculation are given first. Then, coupled-channel results are presented, and the importance of the channels considered are discussed. Finally, summary and discussion are given in Section III.B.

II. THEORETICAL FRAMEWORK

In the current work, we follows the same theoretical frame in the study of the LHCb hidden-charm pentaquarks [26, 27], to study the strange hidden-charm pentaquark. The one-boson-exchange potential of the interactions of strange charmed baryon $\Xi^{(*)c}$ and anticharmed meson $\bar{D}^{(*)}$ is constructed as dynamical kernel. The pseudoscalar $P$, vector $V$ and scalar $\sigma$ exchanges will be considered, and the effective Lagrangian depicting the couplings of light mesons and anticharmed mesons $\bar{D}^{(*)}$ or strange charmed baryons $\Xi^{(*)c}$ are required and will be presented in the below.

A. Relevant Lagrangians

First, we consider the couplings of light mesons and heavy-light anticharmed mesons $\mathcal{P}$ = ($\bar{D}^0$, $D^*$, $D_\gamma^*$). Considering heavy quark limit and chiral symmetry, the Lagrangians have been constructed in the literature as [52–55],

$$L_{H0F} = ig_1(\bar{H}^0\Lambda_{\bar{c}}\sigma_{\mu\nu}H^\mu_0\bar{H}^\nu, )$$

$$L_{HVV} = -i\beta(\bar{H}^0\Lambda_{\bar{c}}\sigma_{\mu\nu}(\gamma^\mu - \partial^\mu\rho_0)\bar{H}^0 + i\lambda(\bar{H}^0\Lambda_{\bar{c}}F_{\mu\nu}(\rho_0)\bar{H}^0),$$

$$L_{H\sigma} = g_3(\bar{H}^0\Lambda_{\bar{c}}\sigma_\Lambda_{\bar{c}}),$$

where $\mathcal{R}$,$\mathcal{V}$ = ($\frac{1}{2}i(\xi\partial_{\mu} - \xi - \xi\partial_{\mu})\bar{P} + \cdots$ is the axial current with $\xi = \exp(i\varphi_1/f_\pi)$ and $f_\pi = 132$ MeV. The vector current $V_\mu = \frac{1}{2}[\xi(\partial_{\mu}\xi) + (\partial^\mu\xi\xi)] = 0$, and vanishes. $\bar{\rho}_{\mu} = ig_2\varphi_{\mu}/\sqrt{2}$, and $F_{\mu\nu}(\rho) = \partial_\mu\rho_j - \partial_j\rho_\mu + [\rho_\mu, \rho_j]$. The $\mathcal{P}$ and $\mathcal{V}$ are the pseudoscalar and vector matrices as

$$\mathcal{P} = \begin{pmatrix}
\frac{1}{2}\rho^0 + \frac{\rho + \rho^0}{\sqrt{2}} & \rho^+ & K^+ \\
\rho^- & K^0 & \frac{\rho - \rho^0}{\sqrt{2}} \\
K^- & \frac{2\rho}{\sqrt{2}} & \frac{\rho^0}{\sqrt{2}} \\
\end{pmatrix},$$

$$\mathcal{V} = \begin{pmatrix}
\frac{\rho^0}{\sqrt{2}} + \frac{\rho - \rho^0}{\sqrt{2}} & \rho^+ & K^+ \\
\rho^- & \frac{2\rho + \rho^0}{\sqrt{2}} & K^0 \\
K^- & \rho^0 & \phi \\
\end{pmatrix}.$$  

(1)

The doublet are defined as $H^\mu_0 = [\rho^0, \rho_{\mu} - \rho_{\mu}\gamma_5]$, and $\bar{H} = \gamma_0 H^* \gamma_0$. The $\mathcal{P}$ and $\mathcal{P}^*$ satisfy the normalization relations $\langle 0|\mathcal{P}|Q\bar{q}(0^+)\rangle = \sqrt{M_\mathcal{P}}$ and $\langle 0|\mathcal{P}^*_\mu|\bar{Q}q(1^-)\rangle = \epsilon_{\mu}\sqrt{M_\mathcal{P}^*}.$

The Lagrangians can be further expanded as follows for explicitly application,

$$L_{P-P'} = \frac{2g}{f_\pi} \frac{\sqrt{m_{P}m_{P'}}}{f_\pi} (-P^\dagger_{a,b}P_{b} + P^\dagger_{a,b}P_{b}) \frac{\partial}{\partial \bar{P}_{ab}},$$

$$L_{P-P} = \frac{g}{f_\pi} \epsilon_{\mu
u}P_{a,b}^{\dagger} \partial_\mu P_{b,a} \bar{P}_{ab},$$

$$L_{P-P'} = \sqrt{2} \bar{\lambda}_V \epsilon_{\mu\nu}\partial_\mu P_{a,b}^{\dagger} \partial_\nu P_{b,a} \bar{P}_{ab},$$

$$L_{P\sigma} = -i\sqrt{2} \bar{\beta}_V \epsilon_{\mu\nu} \partial_\mu P_{a,b}^{\dagger} \bar{P}_{ab} \partial_\nu \sigma_\Lambda_{\bar{c}} \bar{P}_{ab},$$

$$L_{P\sigma} = -i\sqrt{2} \bar{\lambda}_V \epsilon_{\mu\nu} \partial_\mu P_{a,b}^{\dagger} \bar{P}_{ab} \partial_\nu \sigma_\Lambda_{\bar{c}} \bar{P}_{ab},$$

where $\nu$ is replaced by $i\bar{\nu} / 2 \sqrt{m_{\bar{c}}}$ with the $m_{1,2}$ is for the initial or final $D^{(*)}$ meson.

The Lagrangians for the couplings between charmed baryon and light mesons can also be constructed under the heavy quark limit and chiral symmetry as,

$$L_S = \frac{3}{2} g_1 (v_\mu) e^{i\phi}\{ [\bar{S}_\mu, A_1 S_1] + \beta_3 (\bar{S}_\mu v_\mu) G^+ \},$$

$$\bar{S}_\mu = \frac{1}{3} \bar{B}_{ab} \gamma_5 (\gamma^\mu + v_\mu) B_{ab} \equiv \bar{B}_{ab} + B_{ab},$$

and the the bottom baryon matrices are defined as

$$B_3 = \begin{pmatrix}
0 & A_3^+ & \Xi^- \\
-A_3^* & 0 & \Xi^0 \\
-\Xi^+ & -\Xi^0 & 0 \\
\end{pmatrix},$$

$$B' = \begin{pmatrix}
\Sigma^+ & 1 & \Xi^+ \\
1 & \Sigma^0 & \Xi^0 \\
\Xi^+ & \Xi^0 & 0 \\
\end{pmatrix}.$$

(2)

The explicit forms of the Lagrangians can be written as,

$$L_{BBF} = -i \frac{3g_1}{4f_\pi \sqrt{m_{\bar{c}} m_B}} e^{i\phi} \{ \bar{B}_{\mu} \partial_\mu B_\mu \},$$

$$L_{BBV} = -i \frac{\beta_3 g_1}{2 \sqrt{2m_{\bar{c}} m_B}} \gamma^\nu \{ \bar{B}_{\mu} \partial_\mu B_\mu \},$$

$$-i \frac{\lambda_3 g_1}{2 \sqrt{2}} (\partial_\mu \bar{\Lambda}_\nu - \partial_\nu \bar{\Lambda}_\mu) \sum_{i=0,1} \bar{B}_{\mu} B_\mu,$$

(3)
\[ \mathcal{L}_{BB\tau} = \ell_S c^{\tau} \sum_{\nu=0,1} \bar{B}_\nu \gamma^\nu B_\nu, \]
\[ \mathcal{L}_{B_i B_j \nu} = -\frac{g_{\nu \beta}}{2 \sqrt{2m_{B_i}m_{B_j}}} \gamma^\nu \bar{B}_3 \gamma^\mu B_3, \]
\[ \mathcal{L}_{BB_{\nu} \tau} = i \lambda_{BB} B_3, \]
\[ \mathcal{L}_{BB\nu} = -i \frac{g_{\mu \nu}}{f_\pi} \bar{B}_i \gamma^\mu \gamma^\nu \bar{B}_j + \text{H.c.}, \]
\[ \mathcal{L}_{BB_{\nu} \tau} = \frac{g_{\mu \nu} \lambda_{BB}}{2 \sqrt{2m_B m_{B_3}}} e^{\mu \nu \lambda} \partial_\lambda \bar{B}_3 + \text{H.c.}. \] (7)

The masses of particles involved in the calculation are chosen as suggested central values in the Review of Particle Physics (PDG) [56]. The mass of broad \( \sigma \) meson is chosen as 500 MeV. The coupling constants involved are listed in Table I.

\[ \beta \quad g \quad g_v \quad \lambda \quad \lambda_s \]
\[ 0.9 \quad 0.59 \quad 5.9 \quad 0.56 \quad 0.76 \]
\[ \beta_s \quad \ell_S \quad g_1 \quad \gamma_S \quad g_3 \quad \gamma_3 \]
\[ -1.74 \quad 6.2 \quad -0.94 \quad -3.31 \quad -\beta_s \gamma_S / 2 \quad 3g_1 / (2 \sqrt{2}) \quad -\lambda_S / \sqrt{2} \]

With the vertices obtained from above Lagrangians, the potential of couple-channel interaction can be constructed easily with the help of the standard Feynman rules. Because six channels are involved in the current work, it is tedious and fallible to give explicit 36 potential elements and input them into code. Instead, in this work, following the method in Refs. [27], we input vertices \( V \) and propagators \( P \) into the code directly. The potential can be written as

\[ V_{\nu,\tau} = f_1 \Gamma_1 \Gamma_2 P_{\nu,\tau} f(q^2), \quad V_{\nu} = f_1 \Gamma_1 \Gamma_2 P_{\nu,\tau} f(q^2), \] (8)

The propagators are defined as usual as

\[ P_{\nu,\tau} = \frac{i}{q^2 - m_{\nu,\tau}^2}, \quad P_{\nu,\tau} = \frac{i - g_{\nu,\tau} q^\mu / m_{\nu,\tau}^2}{q^2 - m_{\nu,\tau}^2}, \] (9)

where the form factor \( f(q^2) \) is adopted to compress the off-shell effect of exchanged mesons as \( f(q^2) = e^{-m_{\nu,\tau}^2 q^2 / \Lambda_{\nu,\tau}^2} \) with \( m_{\nu,\tau} \) being the appropriate mass and \( q \) being the momentum of the exchanged meson. The \( f_3 \) is the flavor factor for certain meson exchange of certain interaction, and the explicit values are listed in Table II.

| \( D^{(*)} \Xi_l^{(*)} \rightarrow D^{(*)} \Xi_l^{(*)} \) | \( \pi \) | \( \eta \) | \( \rho \) | \( \omega \) | \( \sigma \) |
|-----------------|-----|-----|-----|-----|-----|
| \( \pi^0 \eta^+ \rightarrow \eta^0 \eta^+ \) | \( \frac{1}{2} \) | \( -1 \) | \( -\frac{1}{2} \) | \( \frac{1}{2} \) | \( 1 \) |
| \( \eta^0 \eta^0 \rightarrow \eta^0 \eta^0 \) | 0 | 0 | \( -\frac{1}{2} \) | \( \frac{1}{2} \) | 2 |
| \( \eta^0 \eta^0 \rightarrow \eta^0 \eta^0 \) | \( -\frac{1}{2} \) | \( -\frac{1}{2} \) | \( \frac{1}{2} \) | \( \frac{1}{2} \) | 0 |

With the potential kernel obtained, we adopt the qBSE to solve the scattering amplitude [30, 31, 60–62]. After partial-wave decomposition and spectator quasipotential approximation, the 4-dimensional Bethe-Salpeter equation in the Minkowski space can be reduced to a 1-dimensional equation with fixed spin-parity \( J^P \) as [61],

\[ i M_{F \chi}(p', p) = i V_{F \chi}(p', p) + \sum_{\lambda'} \int \frac{d^2 p''}{(2\pi)^3} \left. \cdot i V_{F \chi}(p', p'') G_0(p'') i M_{F \chi}(p'', p) \right|_{p'' = p'} \] (10)

where the sum extends only over nonnegative helicity \( \lambda' \). The \( G_0(p'') \) is reduced from the 4-dimensional propagator under quasipotential approximation as \( G_0(p'' = \delta^3(p'' - m_h^2) / (p'' - m_h^2)^2 - m_h^2) \) with \( m_h \) and \( m_h' \) being the momenta and masses of heavy or light constituent particles. The partial wave potential is defined with the potential of interaction obtained in the above Eq. (8) as

\[ V_{F \chi}(p', p) = 2\pi \int d\cos \theta \left[ d_{F \chi}^{J l}(\theta) V_{F \chi}(p', p) \right. + \eta d_{F \chi}^{J l}(\theta) V_{F \chi}(p', p) \left|_{p'' = p'} \right. \] (11)

where \( \eta = PP_1 P_2(-1)^{I-I'-I''} \) with \( P \) and \( J \) being parity and spin for system, \( D^{(*)} \) meson or \( \Xi^{(*)} \) baryon. The initial and final relative momenta are chosen as \( p = (0, 0, 0) \) and \( p' = (p' \sin \theta, 0, p' \cos \theta) \). The \( d_{F \chi}^{J l}(\theta) \) is the Wigner d-matrix. We also adopt an exponential regularization by introducing a form factor into the propagator as [61] \( G_0(p'') \rightarrow G_0(p'') \left[ e^{-(p'' - m_h^2)^2 / \Lambda_{F \chi}^2} \right] \) with \( \Lambda_{F \chi} \) being a cutoff.

### III. RESULTS AND DISCUSSIONS

With the preparation above, we can perform numerical calculation to study the molecular states from the \( \Xi^{(*)} D^{(*)} \) and \( \Xi^{(*)} \Xi^{(*)} \) interactions. After transformation of the qBSE into a matrix equation, the scattering amplitude can be obtained, and the molecular states can be searched for as the poles in the complex energy plane. As said in the Introduction, the parameters of the Lagrangians in the current work are chosen as same as those in our previous study of the hidden-charm pentaquarks [26, 27]. The only parameters are cutoff \( \Lambda_{F \chi} \) and \( \Lambda_{F \chi} \), which are rewritten as a form of \( \Lambda_e = \Lambda_{F \chi} = m + \alpha 0.22 \text{ GeV} \). Hence, in the current work, only one parameter is involved, and its value will be discussed later. In the followings, the single-channel results will be presented first. Then, the coupled-channel effects are included to produce the width of the molecular states. The couplings of molecular states to the considered channels are also discussed to analyze the contributions of decay channels.

#### A. Single-channel results

For the six channels considered, the results of single-channel calculation are shown in Fig. 1. All states which can
As shown in the figure, five isoscalar bound states with spin parity $I^P=1^−$ are produced from the $\Xi_c^*$ and the $\Xi_c^′$ interactions. All possible molecular states can be produced in $S$, $P$, and $D$ wave with isospin $I=0$ or $I=1$. All single-channel results of the $\Xi_c^*$ and the $\Xi_c^′$ are also included. The single-channel results and position of poles in Table I are the best candidates for the $\Xi_c^*$ and the $\Xi_c^′$ molecules in the single-channel calculation. The coupled-channel results are expected to be close to the single-channel results. The coupling constants between different channels are not included in the coupled-channel calculation. The coupled-channel results are expected to be close to the single-channel results. The coupling constants between different channels are not included in the coupled-channel calculation.
inclusion of the coupled-channel effect makes the two states from the \(\Xi^- D^+\) interaction deviate from each other. The state with spin parity \(3/2^-\) moves further while the state with \((1/2^-)\) closer to the \(\Xi^- D^+\) threshold. The higher state \(\Xi^- D^+(1/2^-)\) has a mass of 4470.1 MeV. Though two states are separated by the coupled-channel effect, the small mass gap about 10 MeV requires high precision measurement to distinguish these two states in experiment.

With the \(P_{1/2}(4459)\) reproduced in our theoretical framework, we can provide the prediction of other possible strange hidden-charm molecular states. Two states with spin parity \(1/2^-\) are produced near the \(\Xi^- D^-\) and \(\Xi^+ D^-\) thresholds, respectively. The lowest state has zero width because no channel lower than the \(\Xi^- D^-\) threshold is considered in the current work. The state near the \(\Xi^+ D^-\) threshold has a negligible width due to its very weak coupling to the \(\Xi^- D^-\) channel. No \(3/2^-\) state is given here because we only consider the state which can be produced in \(S\) wave. A state can be found near the \(\Xi^+ D^-\) threshold with spin parity \(3/2^-\) with a width of about 14 MeV at \(\alpha\) of a value 3 as shown in Table III. Two poles can also be found near the \(\Xi^+ D^+\) threshold with spin parities \(1/2^-\) and \(3/2^-\). The widths of this two states are similar, and the mass gap is about 5 MeV. Near the highest threshold \(\Xi^+ D^+\), two states can be also produced from the interaction. However, as two \(\Xi^+ D^+\) states predicted in the hidden-charm sector [27], the signal of these two states are very weak as shown in Fig. 2. As shown in Table III, with a larger cutoff, the pole of state with \(3/2^-\) is even difficult to be read out from the results. These two states may be difficult to be observed in experiment.

C. The widths of the molecular states from each decay channel

In the above, we present the widths of the states with all channels considered. The width of a molecular state is from decaying into the channels with thresholds lower than the mass of the state. The width from one of decay channels of a molecular state shows the strength of the couplings between the molecular state and the corresponding channel. By comparing the single and coupled channel results, one can find the coupled-channel effects are not very large. Hence, the main production channel of a molecular can be easily determined by the nearest threshold. In Table IV, we present the pole obtained by a two-channel calculation with main production channel and a decay channel to show the coupling of a molecular state to the decay channel.

![Diagram](image)

**FIG. 2:** The log \(|1 - V(z)G(z)|\) with the variation of \(z\) for the \(\Xi^- D^+\) and \(\Xi^+ D^+\) interaction with \(J^P = 1/2^-\) and \(3/2^-\) at \(\alpha = 3.0\). The color means the value of log \(|1 - V(z)G(z)|\) as shown in the color box.
In the table, the results for the $\Xi^0 D^*$ state near the highest threshold with $1/2^-$ are listed first. Among five decay channels listed in the second to sixth columns, the strongest coupling is found in $\Xi^0 D$ channel. The $\Xi^0 D^*$ is the most important decay channel of the $\Xi^0 D^*$ state with $3/2^-$, and the $\Xi^0 D^*$ and $\Xi D^*$ channels also have considerable contribution to its width. The $\Xi D^*$ channel is also the main decay channel of the molecular states $\Xi D^*(3/2^-, 3/2^-)$ and $\Xi D^*(3/2^-)$. For the $\Xi D^*$ states with $1/2^-$ and $3/2^-$, the $\Xi D$ channel is dominant to produce their widths. The $\Xi D^*(1/2^-)$ state couples to its only open channel $\Xi D$ very weakly. Hence, the $\Xi^0 D^*$ and $\Xi D^*$ channel are important for the decays of four and three molecular states, respectively.

IV. SUMMARY

In this work, the strange hidden-charm pentaquarks are studied in the molecular picture in the qBSE approach. The newly observed state $P_{c+}(4459)$ could be interpreted as the $\Xi^0 D^*(3/2^-)$ molecular state, which has strong coupling to $\Xi D$ channel. The pole of this state is much more obvious in the complex energy plane than other states, which may be the reason that it was observed first. Our result does not exclude the possibility that the $P_{c+}(4459)$ is a two-peak structure composed of the $\Xi^0 D^*$ states with $1/2^-$ and $3/2^-$, which is helpful to understand the experimental width. The current work is performed in the same theoretical frame as previous study of the hidden-charm pentaquarks with almost the same parameters [26]. Hence, the four hidden-charm pentaquarks, $P_{c+}(4312), P_{c+}(4380), P_{c+}(4440), P_{c+}(4457)$, and the strange hidden-charm pentaquark $P_{c+}(4459)$ can be interpreted well in the molecular picture and assigned as $S$-wave state from the interaction of the (strange) charmed baryon and anti-charmed meson.

In the same model, we also predict other possible strange hidden-charm pentaquarks. Two states with spin parity $1/2^-$ are predicted near the $\Xi^0 D$ and $\Xi D^*$ thresholds, respectively. Since the decay channels of these two states are less than other states, their widths may be smaller. Near the $\Xi D$ threshold, an obvious pole can be found in the complex energy plane with $3/2^-$. This state couples strongly with $\Xi D$ channel. As two states near the $\Xi D^*$ threshold, one can find two states with $1/2^-$ and $3/2^-$ near the $\Xi D^*$ threshold, which have strong coupling to the $\Xi D^*$ channel. The poles can also be found near the highest threshold $\Xi^0 D^*$. Such poles are dimly in the complex energy plane, and may be difficult to be find in experiment. The experimental research of those states are helpful to understand the origin of the $P_{c+}$ and $P_c$ states.

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