Indentation modulus extrapolation and thickness estimation of ta-C coatings from nanoindentation

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ABSTRACT

Coatings used in tribological applications often exhibit high hardness and stiffness to achieve high wear resistance. One coating characterization method frequently used is nanoindentation which allows the determination of indentation hardness and indentation modulus among other material properties. The indentation modulus describes the elastic surface behavior during indentation and is, among hardness, a direct indicator for wear resistance. To obtain the true indentation modulus of a coating, it must be measured with varying loads and then extrapolated to zero load. Current recommendation of the standard ISO 14577-4:2016 is a linear extrapolation which fits poorly for nonlinear curves. Such nonlinear curves are commonly found for high hardness mismatches between coating and substrate, for example, superhard tetrahedral amorphous carbon coatings (ta-C) on a steel substrate. In this study, we present a new empirical fit model, henceforth named Sigmoid. This fit model is compared to several existing fit models described in the literature using a large number of nanoindentation measurements on ta-C coatings with wide ranges of indentation modulus and coating thickness. This is done by employing a user-independent and model agnostic fitting methodology. It is shown that the sigmoid model outperforms all other models in the combination of goodness of fit and stability of fit. Furthermore, we demonstrate that the sigmoid model’s fit parameter directly correlates with coating thickness and thus allows for a new approach of determining ta-C coating thickness from nanoindentation.
Introduction

Nanoindentation

Usually, the indentation modulus \( E_{IT} \) can be reliably measured with the Oliver–Pharr method from the unloading curve [1]. For coated materials, a correct measurement of \( E_{IT} \) is hindered by the substrate’s influence. The elastic deformation field has a theoretically unlimited range, and even sample areas far away from the indent position have an influence on the indentation depth. Therefore, unlike hardness it is not possible to give a limit where the substrate influence can be neglected. For this reason, the indentation standard ISO 14577 part 4 [2] describes a method how the pure \( E_{IT} \) of the coating can be obtained. It requires a series of indentation measurements with different forces and depths and the extrapolation of the function \( E_{IT}(a) \) or the normalized function \( E_{IT}(a/t_c) \) to zero depth with \( a \) as contact radius and \( t_c \) as coating thickness. According to the standard [2], a minimum of 10 indents should be performed per force and thus at least 50 measurements are required. This is a relatively time-consuming procedure; therefore, other methods have been developed:

- Cyclic load–unload measurement,
- Continuous stiffness measurement,
- Quasi-continuous stiffness measurement.

In the standard, a linear fit is recommended for simplicity but also nonlinear fit methods are permitted.

Cyclic load-unload measurement

In cyclic load–unload measurements (also called load/partial unload), the contact stiffness can be determined for every unload cycle and give therefore as many modulus results over depth as cycles. The analysis is done in the same way as single load–unload measurements. The method reduces the overall measurement time and number of measuring points, while the technique is realizable with nearly every nanoindentation system. However, the test time per test position is still long and therefore the thermal drift of the instrument has a larger influence and needs to be corrected. In case of a nonlinear thermal drift, the accuracy is reduced, especially for the first cycles at low loads.

Continuous stiffness measurement

The continuous stiffness measurement (CSM) method superimposes a small harmonic oscillation \( \delta F \) to the loading force. By measuring the displacement oscillation \( \delta h \) and the phase angle between force and displacement oscillation, one can obtain the contact stiffness for any point on the load–displacement curve and therefore also the depth-dependent \( E_{IT} \). The method was patented in 1989 by Oliver and Pethica [3] and thus for a long time only available for one instrument type. Today, the patent has expired and most nanoindentation instruments offer dynamic test capabilities. The disadvantage of the method is that only a few oscillation data points are available for every point in the curve and that, due to the quasistatic loading, any oscillation ends at a slightly higher force level than its start level and the oscillation cycle is not fully complete. However, the application of this method was a large progress regarding the extraction of the correct modulus for thin coatings.

Quasi-continuous stiffness measurement

The quasi-continuous stiffness measurement (QCSM) method was developed by Chudoba as an alternative to the CSM method. Here, the load is increased in a stepwise manner without any oscillation, and the oscillation is only switched on during a short dwell time after every load step as shown in Fig. 1. This has the advantage that the feedback during the force application is not influenced by any oscillation and...
that force controllability is improved. During the dwell time of 0.5–3 s (depending on frequency), the average force is constant and oscillations can be averaged easily because the oscillation cycle is always finished at the same force level. This method has therefore a smaller measurement error than both CSM and the cyclic load–unload measurement method and the scatter of the results is small—down to a few-nanometer indentation depth. Further, a very good agreement to test results of conventional load–unload cycles could be achieved without additional corrections. The typical number of 30–40 points in one load segment is smaller than for the CSM method but larger than for cyclic measurements. It is also high enough for a good presentation of the depth dependency of the modulus for coated materials.

**Models for fitting indentation modulus–displacement curves**

Most of the alternative models for fitting the \( E_{IT} - a \) data can be grouped into two basic forms: linear additive Eq. (1) and reciprocal additive Eq. (2).

\[
E_{IT} = E_{IT,1} + (E_{IT,2} - E_{IT,1}) \cdot \phi_l
\]

\[
\frac{1}{E_{IT}} = \frac{1}{E_{IT,1}} + \left( \frac{1}{E_{IT,2}} - \frac{1}{E_{IT,1}} \right) \cdot \phi_r
\]

\( \phi \) is the model-specific weight function which is set up to approach the coating indentation modulus \( E_{IT,c} \) for \( a = 0 \) and the substrate indentation modulus \( E_{IT,s} \) for \( a \to \infty \). Accordingly, \( E_{IT,1} \) and \( E_{IT,2} \) describe model-dependent substrate and coating indentation moduli. \( k \) is an additional fit factor.

The fit models listed in Table 1 were compiled and modified from the literature. Models dependent on \( h \) have been changed to a function of \( a \) where necessary to achieve independency from the indenter geometry. **Linear**, **Exponential**, and **Reciprocal Exponential** use empirical \( \phi \). These fit models have first been described by Menčík et al. for fitting \( E_{IT} - a \) curves [4]. The other models follow theoretical considerations. **Linear** describes the linear fit according to ISO 14577-4:2016 [2].

**Gao1** and **Gao2** were originally based on thoughts by Gao et al. on the elastic indentation behavior of a flat, cylindrical punch into a solid surface [5]. **Gao2** has later successfully been applied to a pyramidal indenter by Menčík et al. without modification [4].

**Puchi-Cabrera** has first been proposed by Antunes et al. who transformed the linear additive form of **Gao2** into a reciprocal additive one while keeping \( \phi \) [6]. The listed version with a modified \( \phi \) has been published by Puchi-Cabrera et al. [7].

**Bull** has been proposed by Bull according to his geometrical consideration of the loading of a coated substrate [8]. He theorizes the development of a supporting volume beneath the contact which is shaped like a truncated cone. Originally, it has been formulated with substrate thickness \( t_s \) and coating thickness \( t_c \) as follows:

\[
E_{IT} = \left[ E_{IT,c}^{-1} \left( 1 - \frac{\pi a}{\pi a + 2t_c} \right) \right]^{-1}
\]

For the investigated samples, \( t_s \gg t_c \) holds true, so the last term can be truncated:

\[
\frac{\pi a}{\pi a + 2t_c} = \frac{\pi a}{\pi a + 2(t_c + t_s)} \approx \frac{\pi a}{\pi a + 2t_c}
\]

Additionally, \( t_c \) is assigned as a second fit parameter.

**Linear**, **Exponential**, and **Reciprocal Exponential** have originally referred to \( a/t_c \). In these cases, \( t_c \) is included in the second fit parameter \( k \) since both are constant for a given sample. This is done so that all fit models have the same degree of freedom which increases comparability and also eliminates the need to measure \( t_c \). The inclusion of \( t_c \) furthermore would introduce an additional source of error. In contrast, for **Gao1** and **Gao2**, the coating thickness is used as an additional free fit parameter to conform to the requirement of two fit parameters.

Additional fit models described by Menčík et al. [4] and Doerner and Nix [9] were not considered due to their unsuitable curve progression.

These models could not adequately describe the QCSM results of our samples; thus, we propose a new fit model for an improved extrapolation. It is based on the linear additive form Eq. (1) with \( E_{IT,3} = E_{IT,c} \) and henceforth labeled **Sigmoid**.

The Oliver–Pharr method on its own cannot provide the necessary extrapolation for extracting \( E_{IT,c} \). For an overall impression, all introduced fit models are fitted to one sample in Fig. 2. It is apparent that the unique curve progression of every model is resulting in a different goodness of fit.
Tetrahedral amorphous hydrogen-free carbon

Hydrogen-free tetrahedral amorphous carbon (ta-C) is a form of amorphous carbon (sometimes called diamond-like carbon (DLC)) with a high degree of sp³-hybridized atoms exceeding 50%. The degree of sp³-hybridized atoms determines properties such as density, \( H_{IT} \), and \( E_{IT} \) [10], making ta-C the hardest type of amorphous carbon. ta-C coatings can be produced by physical vapor deposition techniques that provide high ionization of the carbon. The coatings investigated in this study were deposited by an industry-scale laser-induced pulsed vacuum arc technique (LaserArc) [11, 12]. This method allows to vary the degree of sp³ hybridization and thus coating properties in a wide range of 20–80 GPa \( H_{IT} \). In addition to its outstanding mechanical properties, ta-C coatings show a beneficial tribological behavior (low friction, low wear) that causes its application as friction-reducing coatings and/or wear protection coating in highly stressed parts, i.e., in automotive applications [13, 14]. The high \( E_{IT} \) of ta-C results in strongly curved \( E_{IT}/C_0 \) curves when deposited on conventional steel substrates as shown in Fig. 3.

Materials and methods

Samples

All samples were prepared by coating polished disks with ta-C in a Laser-Arc-PVD process. These disks were made of hardened low-alloy chromium steel (100Cr6, EN 1.3505, approximately HRC 60). Measurements were conducted on 55 different coating batches. The coatings ranged from \( t_c = 0.7 \) to 25 \( \mu \)m and...
indentation hardness $H_{IT} = 13$ to 74 GPa. The roughness of ta-C coatings is influenced by their thickness, so the sample surfaces were polished lightly (typically $R_a \leq 20$ nm) for comparable measurements.

NANOINDENTATION

All nanoindentation measurements were performed on a nanomechanical testing system Zwick/Roell ZHN using a Berkovich indenter with a nominal tip rounding of less than 200 nm. The device was used in QCSM mode with 30 points of measurement during loading, 40 Hz frequency, and 100 mN maximum load. The area function was calibrated at least every three samples. The $v$ for ta-C was assumed to be 0.19 [15]. Every sample measurement is comprised of the mean of at least ten individual measurements excluding outliers identified by the device software.

Fit model comparison criteria

For comparing the fit models, we chose two criteria whose relevance will be outlined as follows:

- Goodness of fit,
- Stability of fit.

Goodness of fit

Due to the quantity of different fit models, a preselection of the considered fit range could not be made. Instead, the models were evaluated over several $a/t_c$ ranges. The total size of the fit range was fixed at 0.25. This range was established empirically as a good compromise between as many measurement points as possible from each individual measurement, while including as many different samples as possible, where measurement with large contact radius becomes the limit. Starting at a lower limit of $a/t_c = 0$ and a corresponding upper limit of $a/t_c = 0.25$, the fit range was moved incrementally over the whole curve and a new $E_{IT,c}$ calculated for every sample and fit model. Examples are given in Fig. 4. To compare the fit models, for every fit range the mean $<c_v^2>$ over all samples was calculated with a custom-written software tool for all fit model–fit range combinations.

Stability of fit

For minimizing the operator influence, the extrapolated $E_{IT,c}$ should be stable for a wide range. Particularly, small changes of the number and position of the measuring points should not cause larger changes in the extrapolated value. Equivalent to the approach for evaluating the goodness of fit, the stability of fit was examined over a variable fit range. For every sample and fit model, the fit range-dependent coefficient of variation $c_v(E_{IT,c})$ was calculated. Then, the mean of $c_v(E_{IT,c})$ over all samples was calculated to produce the mean coefficient of variation $<c_v(E_{IT,c})>$.
Results and discussion

Comparison of fit models

Goodness of fit

\(<v^2_{\text{red}}>\) is shown in Fig. 5 for all fit models up to [0.25, 0.5]. The proposed \textit{SIGMOID} shows the best fit, with \textit{LINEAR} showing an equally good fit from [0, 0.25] to [0.1, 0.35]. \textit{EXPONENTIAL} shows a comparable, albeit slightly worse fit over all fit ranges compared to \textit{SIGMOID}. Despite its linear character which cannot follow the curved progression, \textit{LINEAR} performed better than most other models. This is surprising but can be explained by these other models being unsuited for our ta-C samples. Fit ranges with an upper bound higher than 0.5 were not considered due to the unreasonably high load necessary for thick or hard samples to reach this threshold. Out of 55 measurements, only 11 exceeded \(a/t_c = 0.5\).

Stability of fit

The calculated \(<c_v(E_{IT, c})>\) values for every fit model are listed in Table 2. Due to the fit guidance from \(E_{IT, c}\), most models showed a reasonably good stability of fit. Still, there were occasional instabilities for smaller amounts of fitted points which manifested themselves in a considerable higher \(E_{IT, c}\) extrapolation compared to the higher fit regions and therefore higher \(<c_v(E_{IT, c})>\). This is demonstrated in Fig. 6. Only \textit{LINEAR}, \textit{SIGMOID}, and \textit{EXPONENTIAL} were able to extrapolate a stable \(E_{IT, c}\) over all ranges. Accordingly, these had equally the lowest \(<c_v(E_{IT, c})>\) with \textit{RECIPROCAL EXPONENTIAL} trailing closely behind. All other fit models’ \(<c_v(E_{IT, c})>\) were at least four times higher. \textit{RECIPROCAL EXPONENTIAL}’s instability described by Menčík [4] could not be confirmed.

Correlation of coating thickness

The \textit{SIGMOID} fit factor \(k\) is connected to \(t_c\) since it describes the fit curve steepness. The thinner the measured coating, the higher the fitted curve’s slope (and thus \(k\)) since it approaches the substrate value more quickly. For thin coatings, it approaches fast, leading to a large \(k\). For thick coatings, \(E_{IT}\) approaches \(E_{IT, s}\) much slower, corresponding to a small \(k\). This relationship is particularly strong for ta-C,

\begin{table}[h]
\centering
\begin{tabular}{|l|l|}
\hline
Fit model & \(<c_v(E_{IT, c})>\) \\
\hline
\textit{SIGMOID} & 0.08 \\
\textit{LINEAR} & 0.07 \\
\textit{EXPONENTIAL} & 0.10 \\
\textit{RECIPROCAL EXPONENTIAL} & 0.19 \\
\textit{Gao1} & 0.72 \\
\textit{Gao2} & 0.90 \\
\textit{BULL} & 3.41 \\
\textit{PUCHI-CABRERA} & 2.55 \\
\hline
\end{tabular}
\caption{Comparison of stability of fit for the researched fit models. A lower \(<c_v(E_{IT, c})>\) means lower variation of the extrapolated \(E_{IT, c}\) when varying the fit boundaries which implies a more stable fit.}
\end{table}

\begin{figure}[h]
\centering
\includegraphics[width=\textwidth]{fig6.png}
\caption{Comparison of extrapolated \(E_{IT, c}\) for all considered fit models.}
\end{figure}
which shows only little disruptive plastic deformation. \( k \) as a function of \( t_c \) is shown in Fig. 7 for the investigated samples. Because of the assumed inverse correlation of fit factor and coating thickness, a fit curve according to Eq. (5) is proposed.

\[
k = \frac{c}{t_c}
\]  

(5)

\( c \) describes a coating thickness factor specific to the coated system and amounts to \( 3.139 \pm 0.021 \) for the investigated ta-C coatings on steel. Accordingly, with known \( k \) and \( c \) one can calculate a measured coating’s thickness with Eq. (6).

\[
t_{\text{calc}} = \frac{3.139}{k} \Delta t_{\text{calc}} = \frac{0.021}{k} 1 + \Delta k \frac{3.139}{k^2}
\]  

(6)

This relation enables the determination of coating thickness by evaluating QCSM measurements with the sigmoid fit model. The resulting errors for the whole sample set employing Eq. (6) are shown in Fig. 8. The relative error \( \Delta t_{\text{calc}}/t_c \) is consistently smaller than 20% for \( t_c \) thinner than 2 \( \mu \)m. The fitting error can be improved by increasing \( h \) with higher \( F_{\text{max}} \).

### Conclusions

This work introduces the SIGMOID fit model for the extrapolation of the coating indentation modulus \( E_{IT,c} \) and evaluates this model along with several other models compiled from the literature. For this, a broad data basis was established by measuring 55 steel samples coated with ta-C with \( t_c = 0.7 \) to 25 \( \mu \)m and \( E_{IT,c} = 130 \) to 740 Gpa with the QCSM method. All methods were evaluated with an in-house software tool regarding goodness of fit and stability of fit. The resulting assessment is given in Table 3. The newly proposed SIGMOID fit model has the best fit quality with reduced influence of the considered fit range. SIGMOID and LINEAR can be recommended for different use cases, and an assessment is given in Table 4.

In addition, an empirical approach is demonstrated which allows for a nondestructive coating thickness estimate from depth-resolved \( E_{IT} \) curves. This method is applicable even for small samples and complex geometries and is best used for thinner coatings since the error grows with \( t_c \). While the method is demonstrated for ta-C coatings, other coating systems would require the determination of a

| Model               | Goodness of fit | Stability of fit |
|---------------------|-----------------|------------------|
| SIGMOID             | ++              | ++               |
| LINEAR              | +               | +                |
| EXPONENTIAL         | ++              | ++               |
| RECIPROCAL EXPONENTIAL | –      | –                |
| Gao1                | –               | –                |
| Gao2                | –               | –                |
| Puchi-Cabrera       | –               | –                |
| Bull                | –               | –                |

Table 3 Fit model comparison; + positive assessment; – negative assessment.
new correlation factor with the outlined method. Additionally, the correlation can be used to confirm fit correctness of a Sigmoid fit to a ta-C QCSM curve by comparing correlated and expected thickness.

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### Declarations

**Conflict of interest** The authors declare that they have no conflict of interest.

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