Magnetic anisotropy in (Ga,Mn)As: Influence of epitaxial strain and hole concentration

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We present a systematic study on the influence of epitaxial strain and hole concentration on the magnetic anisotropy in (Ga,Mn)As at 4.2 K. The strain was gradually varied over a wide range from tensile to compressive by growing a series of (Ga,Mn)As layers with 5% Mn on relaxed graded (In,Ga)As/GaAs templates with different In concentration. The hole density, the Curie temperature, and the relaxed lattice constant of the as-grown and annealed (Ga,Mn)As layers turned out to be essentially unaffected by the strain. Angle-dependent magnetotransport measurements performed at different magnetic field strengths were used to probe the magnetic anisotropy. The measurements reveal a pronounced linear dependence of the uniaxial out-of-plane anisotropy on both strain and hole density. Whereas the uniaxial and cubic in-plane anisotropies are nearly constant, the cubic out-of-plane anisotropy changes sign when the magnetic easy axis flips from in-plane to out-of-plane. The experimental results for the magnetic anisotropy are quantitatively compared with calculations of the free energy based on a mean-field Zener model. An almost perfect agreement between experiment and theory is found for the uniaxial out-of-plane and cubic in-plane anisotropy parameters of the as-grown samples. In addition, magnetostriction constants are derived from the anisotropy data.

Keywords: (Ga,Mn)As; (In,Ga)As; Strain; Magnetic anisotropy; Magnetotransport

I. INTRODUCTION

Spin-related phenomena in semiconductors, such as spin polarization, magnetic anisotropy (MA), and anisotropic magnetoresistance (AMR), open up new concepts for information processing and storage beyond conventional electronics. Being compatible with the standard semiconductor GaAs, the dilute magnetic semiconductor (Ga,Mn)As has proven to be an ideal playground for studying future spintronic applications. In particular, the pronounced MA and AMR, largely arising from the spin-orbit coupling in the valence band, potentially apply in novel non-volatile memories and magnetic-field-sensitive devices. Ferromagnetism is implemented in (Ga,Mn)As by incorporating high concentrations (\( \gtrsim 1\% \)) of magnetic Mn\(^{2+}\) ions into the Ga sublattice. The ferromagnetic coupling between the S=5/2 Mn spins is mediated by itinerant holes provided by the Mn acceptor itself. Curie temperatures \( T_C \) up to 185 K, i.e. well above the liquid-N\(_2\) temperature, have been reported and there is no evidence for a fundamental limit to higher values.

The magnetic properties of (Ga,Mn)As are strongly temperature dependent and can be manipulated to a great extent by doping, material composition, and strain. In (Ga,Mn)As grown on GaAs substrates, however, hole density \( p \), Mn concentration \( x \), and strain \( \varepsilon \) are intimately linked to each other and cannot be tuned independently by simply varying the growth parameters. \( p \) and \( \varepsilon \) sensitively depend on the concentration and distribution of the Mn atoms which are incorporated both on Ga lattice sites (Mn\(_{Ga}\)) and, to a lower extent, on interstitial sites (Mn\(_i\)), where they act as compensating double donors. Post-growth treatment techniques such as annealing or hydrogenation are frequently used to increase or decrease the hole concentration due to outdiffusion and/or rearrangement of Mn\(_{Ga}\) or due to the formation of electrically inactive (Mn,H) complexes, respectively. In both cases, however, the treatment concurrently leads to a decrease or increase of the lattice parameter, respectively, and thus to a change of the strain.

The epitaxial strain in the (Ga,Mn)As layers, arising from the lattice mismatch between layer and substrate, can be adjusted by tailoring the lattice parameter of the substrate. While (Ga,Mn)As grown on GaAs is under compressive strain, tensily strained (Ga,Mn)As can be obtained by using appropriate (In,Ga)As/GaAs templates. Experimental studies addressing this issue, however, have so far been restricted to merely a limited number of representative samples.

In this work, the influence of epitaxial strain and hole concentration on the MA at 4.2 K is analyzed in a systematic way by investigating a set of (Ga,Mn)As layers grown on relaxed (In,Ga)As/GaAs templates with differ-
ent In concentration. Keeping the Mn content at ~5% and changing the maximum In content in the (In,Ga)As buffer layers from 0% to 12%, the vertical strain $\varepsilon_{zz}$ in the as-grown (Ga,Mn)As layers could be gradually varied over a wide range from $\varepsilon_{zz}=0.22\%$ in the most compressively strained sample to $\varepsilon_{zz}=-0.38\%$ in the most tensely strained sample without substantially changing $p$. Post-growth annealing leads to an increase in $p$, yielding a second series of samples with nearly the same range of $\varepsilon_{zz}$ but higher hole concentrations. The strain dependence of the anisotropy parameters for the as-grown and the annealed samples was determined by means of angle-dependent magnetotransport measurements. Part of the experimental data has already been published in conference proceedings. Here, we combine the earlier with the present extensive experimental findings advancing a quantitative comparison of the intrinsic anisotropy parameters with model calculations for the MA, performed within the mean-field Zener model introduced by Dietl et al. Note that several samples analyzed in Ref. 23 have been substituted by new samples grown under optimized conditions and that the sample series has been expanded by one specimen with $\varepsilon_{zz}=-0.38\%$.

II. EXPERIMENTAL DETAILS

A set of differently strained (Ga,Mn)As layers with constant Mn concentration of ~5% and thickness of ~180 nm was grown by low-temperature molecular-beam epitaxy (LT-MBE) on (In,Ga)As/GaAs templates with different In content in a RIBER 32 MBE machine. Indium-mounted semi-insulating VGF GaAs(001) wafers were used as substrates. After thermal deoxidation, a 30-nm-thick GaAs buffer layer was deposited at a substrate temperature of $T_s \approx 580 \, ^\circ C$. Then the growth was interrupted, $T_s$ was lowered to ~130 °C, and a graded (In,Ga)As buffer with a total thickness of up to ~5 $\mu$m was grown. Starting with In$_{0.05}$Ga$_{0.95}$As, the temperature of the In cell was first continuously raised to increase the In content up to a value of $\leq 12\%$ and was then kept constant until the required thickness of the buffer layer was reached. The growth was again interrupted, $T_s$ was lowered to ~250 °C, and the (Ga,Mn)As layer was grown in As$_4$ mode at a growth rate of ~200 nm/h. The growth was monitored by reflection high-energy electron diffraction showing no indication of a second-phase formation. The use of a graded (In,Ga)As buffer minimizes the deterioration of the (Ga,Mn)As layer caused by threading dislocations in the relaxed (In,Ga)As/GaAs template. The resulting (Ga,Mn)As layers exhibit nearly the same quality as conventional samples directly grown on GaAs. After the growth, the samples were cleaved into several pieces and some of the pieces were annealed in air for 1 h at 250 °C. The structural properties of the (Ga,Mn)As layers were analyzed by means of high-resolution x-ray diffraction (HRXRD) measurements performed with a Siemens D5000HR x-ray diffractometer using the Cu-K$_{\alpha1}$ radiation at 0.154 nm. Hall bars with current directions along the [100] and [110] crystallographic axes were prepared from the samples by standard photolithography and wet chemical etching. The width of the Hall bars is 0.3 mm and the longitudinal voltage probes are separated by 1 mm. The hole densities were determined by high-field magnetotransport measurements (up to 14.5 T) at 4.2 K using an Oxford SMD 10/15/9 VS liquid-helium cryostat with superconducting coils. The Curie temperatures were estimated from the peak positions of the temperature-dependent sheet resistivities at 10 mT. The MA of the samples was probed by means of angle-dependent magnetotransport measurements at 4.2 K using a liquid-He bath cryostat equipped with a rotatable sample holder and a standard LakeShore electromagnet system with a maximum field strength of 0.68 T. To determine the saturation magnetization, we employed a Quantum Design MPMS-XL-7 superconducting quantum interference device (SQUID) magnetometer using the Reciprocating Sample Option (RSO). The measured SQUID curves were corrected for the diamagnetic contribution of the substrate.

As discussed in detail in Ref. 27, our samples exhibit spin wave resonances which are most pronounced for the external magnetic field oriented perpendicular to the sample plane. These spin wave excitations have been traced back to an inhomogeneous free-energy density profile, or more precisely to a linear variation of the MA parameters along the growth direction, presumably arising from a vertical gradient in the hole density. Therefore, all physical parameters derived via magnetotransport in this study have to be considered as effective parameters representing the averaged electronic and magnetic properties of the layers.

III. THEORETICAL CONSIDERATIONS

In the present context, MA represents the dependence of the free-energy density $F$ on the orientation $\mathbf{m}$ of the magnetization $\mathbf{M} = M \mathbf{m}$. In the absence of an external magnetic field, $\mathbf{m}$ is determined by the minimum of the free energy. Since for reasons of crystal symmetry $F$ usually exhibits several equivalent minima, more than one stable orientation of $\mathbf{M}$ exists. This symmetry-induced degeneracy of $F$ can be lifted by the application of an external magnetic field $\mathbf{H}$.

The theoretical considerations on the AMR and the MA in this paper are based on a single-domain model with a uniform magnetization $\mathbf{M}$. While the direction of $\mathbf{M}$ is controlled by the interplay of $F$ and $\mathbf{H}$, its magnitude $M$ is assumed to be constant under the given experimental conditions. For sufficiently high field strengths $H$, this assumption can be considered as a good approximation. Hence, the normalized quantity $F_M=F/M$ is considered instead of $F$, allowing for a concise description of the MA.
A. Phenomenological description of the MA

There are several contributions to $F_M$ which we refer to as intrinsic (magnetocrystalline) or extrinsic:

$$F_M = F_{M,\text{int}} + F_{M,\text{ext}} .$$  

(1)

The intrinsic part $F_{M,\text{int}}=F_{M,c}+F_{M,S}$ originates from the holes in the valence band ($F_{M,c}$) (see Sec. III B) and from the localized Mn spins ($F_{M,S}$). Whereas $F_{M,c}$ is strongly anisotropic with respect to the magnetization orientation, reflecting the anisotropy of the valence band, the localized-spin contribution $F_{M,S}=$ integral of $\mu_0 H'(M')/M$ is isotropic and therefore irrelevant for the following considerations. In a phenomenological description, $F_{M,\text{int}}$ can be expressed in terms of a series expansion in ascending powers of the direction cosines $m_x, m_y,$ and $m_z$ of the magnetization with respect to the cubic axes $[100], [010],$ and $[001]$, respectively. Considering terms up to the fourth order in $m$, $F_{M,\text{int}}$ for cubic systems with tetragonal distortion along the $[001]$ growth direction is given by

$$F_{M,\text{int}}(m) = B_0 + B_{2\perp} m_z^2 + B_{4\parallel}(m_x^4 + m_y^4) + B_{4\perp} m_z^4 .$$  

(2)

In the case of a perfect cubic crystal, symmetry requires $B_{2\perp} = 0$ and $B_{4\parallel} = B_{4\perp}$. The extrinsic part $F_{M,\text{ext}}$ comprises the demagnetization energy due to shape anisotropy and a uniaxial in-plane anisotropy along $[110]$. The origin of the latter anisotropy is controversially discussed. It is traced back either to highly hole-concentrated (Ga,Mn)As clusters formed during the growth30 to the anisotropy of the reconstructed initial GaAs (001) substrate surface31 or to a trigonal-like distortion which may result from a nonisotropic Mn distribution, caused, for instance, by the presence of surface dimers oriented along $[110]$ during the epitaxy.32 Approximating the (Ga,Mn)As layer by an infinite plane, we write the total extrinsic contribution as

$$F_{M,\text{ext}}(m) = B_4 m_z^2 + B_{110} \frac{1}{2}(m_x - m_y)^2 ,$$  

(3)

where $B_4 = \mu_0 M/2$.

In the presence of an external magnetic field $H = H_{\text{ext}}$, the normalized Zeeman energy $-\mu_0 H \mathbf{m}$ has to be added to the total free-energy density. This corresponds to a transition from $F_M$ to the normalized free-enthalpy density

$$G_M(\mathbf{m}) = B_0 + (B_{2\perp} + B_4)m_z^2 + B_{4\parallel}(m_x^4 + m_y^4) + B_{4\perp} m_z^4 + B_{110} \frac{1}{2}(m_x^2 + m_y^2)^2 - \mu_0 H \mathbf{m} .$$  

(4)

The anisotropy parameters $B_{2\perp}$ and $B_4$ are both related to $m_z^2$ and are therefore combined into a single parameter $B_{001}$. Given an arbitrary magnitude and orientation of $H$, the direction of $\mathbf{m}$ is determined by the minimum of $G_M$.

All anisotropy parameters introduced above are in SI units. Expressed by the anisotropy fields in cgs units as defined, e.g., in Ref. 33, they read as $B_{110} = -\mu_0 H_{\text{sat}}/2, B_{2\perp} = -\mu_0 H_{\text{sat}}/2, B_{4\parallel} = -\mu_0 H_{\text{sat}}/4, B_{4\perp} = -\mu_0 H_{\text{sat}}/4$. Note also that the magnetic anisotropy field used in Ref. 27 and the anisotropy parameters used here are related via $\mu_0 H_{\text{aniso}} = 2(K_{\text{eff}} + K_{\text{aniso}})/\mu_0$ with that predicted by the mean-field Zener model.

According to the $k \cdot p$ effective Hamiltonian theory presented in Ref. 3, the Hamiltonian of the system is given by

$$\mathcal{H} = \mathcal{H}_{\text{KL}} + \mathcal{H}_e + \mathcal{H}_{\text{pd}} .$$  

(5)

Here, $\mathcal{H}_{\text{KL}}$ represents the $6 \times 6$ Kohn-Luttinger $k \cdot p$ Hamiltonian for the valence band and $\mathcal{H}_e = \sum_{i,j} D^{(ij)} \varepsilon_{ij}$ accounts for the strain $\varepsilon_{ij}$ in the (Ga,Mn)As layer via the deformation potential operator $D^{(ij)}$. $\mathcal{H}_{\text{pd}} = -N_0 \beta S \mathbf{S}$ describes the p-d hybridization of the p-like holes and the localized Mn d-shell electrons, which results in an interaction between the hole spin $\mathbf{s}$ and the Mn spin $\mathbf{S}$ carrying a magnetic moment $S g \mu_B$. Here, $g = 2$ is the Landé factor, $\mu_B$ the Bohr magneton, and $\beta$ and $N_0$ denote the p-d exchange integral and the concentration of cation sites, respectively. In terms of the virtual crystal and mean-field approximation, the exchange interaction can be written as $\mathcal{H}_{\text{pd}} = M_0 \beta S / g \mu_B$. Explicit expressions for the individual contributions in Eq. (5) can be found in Ref. 3. As an approximation, the values of the Luttinger parameters $\gamma_i$ ($i = 1,2,3$), the spin-orbit splitting $\Delta_0$, and the valence band shear deformation potential b are chosen as those of GaAs. Explicit values are $\gamma_1 = 6.85$, $\gamma_2 = 2.1$, $\gamma_3 = 2.9$, $\Delta_0 = 0.34$ eV and $b = -1.7$ eV, respectively. The quantity parameterizing the exchange splitting of the valence subbands is given by

$$B_G = A_F^0 \beta M / 6 g \mu_B ,$$  

(6)

with the Fermi liquid parameter $A_F$. In contrast to Ref. 3, we restrict our calculations to zero temperature ($T=0$) and zero magnetic field ($H=0$). In this approximation, the Fermi distribution is represented by a step
function and the Zeeman as well as the Landau splitting can be neglected. These simplifications are justified, as our measurements were carried out at $T=4.2$ K and $\mu_0 H < 0.7$ T, where the Zeeman and Landau splittings of the valence band are expected to be much smaller than the splitting caused by the p-d exchange coupling. Diagonalization of the Hamilton matrix $\mathcal{H}$ yields the sixfold spin-split valence band structure in the vicinity of the $\Gamma$ point, depending on the magnetization orientation $m$ and the strain $\varepsilon_{ij}$ in the (Ga,Mn)As layer.

The $m$- and $\varepsilon_{ij}$-dependent normalized free-energy density of the carrier system $F_{M,e}(\varepsilon_{ij}, m)$ is obtained by first summing over all energy eigenvalues within the four spin-split heavy-hole and light-hole Fermi surfaces and then dividing the resulting energy density by $M$. The two split-off valence bands do not contribute to $F_{M,e}$ because they lie energetically below the Fermi energy for common carrier concentrations. For biaxially strained (Ga,Mn)As layers grown pseudomorphically on (001)-oriented substrates, the tetragonal distortion of the crystal lattice along [001] can be fully described by the $\varepsilon_{zz}$ component of the strain tensor using continuum mechanics.

In order to compare the microscopic theory with the phenomenological description of the MA in Sec. IIIA we consider the dependence of $F_M$ on $m$ with respect to the reference direction $m_{\text{ref}}=[100]$. Accordingly, we write the anisotropic part $\Delta F_{M,\text{int}}$ of the intrinsic contribution $F_{M,\text{int}}$ as

$$\Delta F_{M,\text{int}} = F_{M,e}(\varepsilon_{zz}, m) - F_{M,e}(\varepsilon_{zz}, [100]).$$  \hspace{1cm} (7)

In terms of the anisotropy parameters from Eq. (2), $\Delta F_{M,\text{int}}$ reads as

$$\Delta F_{M,\text{int}} = B_{2\perp} m_z^2 + B_{4\parallel}(m_x^4 + m_y^4 - 1) + B_{4\perp} m_z^4.$$  \hspace{1cm} (8)

For $m$ rotated in the (001) and the (010) plane, Eq. (8) can be rewritten as

$$\Delta F_{M,\text{int}}(\varphi) = B_{4\parallel}(\cos^4 \varphi + \sin^4 \varphi - 1)$$

and

$$\Delta F_{M,\text{int}}(\theta) = B_{2\perp} \cos^2 \theta + B_{4\parallel}(\sin^4 \theta - 1) + B_{4\perp} \cos^4 \theta,$$  \hspace{1cm} (10)

respectively, where we have introduced the azimuth angle $\varphi$ and the polar angle $\theta$ with $m_x=\sin \theta \cos \varphi$, $m_y=\sin \theta \sin \varphi$, and $m_z=\cos \theta$. We proceed by calculating $\Delta F_{M,\text{int}}$ numerically in the microscopic model as a function of $\varphi$ and $\theta$ with $\varepsilon_{zz}$ varied in the range $-0.4\% \leq \varepsilon_{zz} \leq 0.3\%$, using typical values for $p, B_G$, and $M$. Equations (9) and (10) are then fitted to the resulting angular dependences using $B_{2\perp}$, $B_{4\parallel}$, and $B_{4\perp}$ as fit parameters.

For the hole density we use the value $p=3.5 \times 10^{20}$ cm$^{-3}$, for the exchange-splitting parameter $B_G=-23$ meV, and for the magnetization $\mu_0 M=40$ mT. Inserted into Eq. (10), the latter two values yield $A_F N_0 \beta_{\varepsilon}=1.8$ eV, in good agreement with the parameters used in Ref. [3].

The results of the microscopic calculations are depicted by the solid symbols in Figs. (a) and (b). Since the variation of $\Delta F_{M,\text{int}}(\varphi)$ with $\varepsilon_{zz}$ is found to be marginal, only one representative curve calculated with $\varepsilon_{zz}=-0.4\%$ is shown in Fig. (a). It clearly reflects the fourfold symmetry of $\Delta F_{M,\text{int}}$ within the (001) plane. By contrast, $\Delta F_{M,\text{int}}(\theta)$ in Fig. (b) strongly depends on $\varepsilon_{zz}$. The solid lines in Figs. (a) and (b) are least-squares fits to the calculated data using Eqs. (9) and (10), respectively. The perfect agreement between the microscopic results and the fit curves demonstrates that the intrinsic part of the free energy calculated within the microscopic theory can be well parameterized by $B_{2\perp}$, $B_{4\parallel}$, and $B_{4\perp}$. It thus justifies the phenomenological ap-

FIG. 1: $\Delta F_{M,\text{int}}$ calculated as a function of the magnetization orientation and the strain within the microscopic model (solid symbols) for $M$ (a) in the (001) plane and (b) in the (010) plane. $\varphi$ and $\theta$ denote the azimuth and polar angles of $M$, respectively. The solid lines are least-squares fit curves using (a) Eq. (9) and (b) Eq. (10) with $B_{2\perp}$, $B_{4\parallel}$, and $B_{4\perp}$ as fit parameters. (c) The anisotropy parameter $B_{2\perp}$ obtained from the fit shows a pronounced linear dependence on $\varepsilon_{zz}$. 


proach in Eq. (2), taking into account only terms up to the fourth order in $m$. Whereas the cubic anisotropy parameters $B_{4h} \approx B_{4h} \approx -30 \text{ mT}$ obtained from the fit are not substantially affected by $\varepsilon_{zz}$, the uniaxial parameter $B_{2h}$ exhibits a pronounced linear dependence on $\varepsilon_{zz}$, as shown in Fig. 1(c). The slope of $B_{2h}(\varepsilon_{zz})$ is strongly influenced by the exchange-splitting parameter $B_G$ and the hole density $p$, as will be discussed in more detail in Sec. IV.C (Fig. 2(b)).

The microscopic calculations show that for $\varepsilon_{zz} < 0$ (tensile strain) $\Delta F_M^\text{int}$ exhibits two equivalent minima for $m$ oriented along $[001]$ and $[00\bar{1}]$, which become more pronounced with increasing tensile strain. In contrast, in the regime of compressive strain ($\varepsilon_{zz} > 0$), the minima occur for $m$ along $[100]$, $[100]$, $[010]$, and $[010]$. Thus, the theoretical model correctly describes the well known experimental fact that for sufficiently high hole densities and low temperatures the magnetically hard axis along $[001]$ in compressively strained layers turns into an easy axis in tensily strained layers. Note, however, that for a quantitative comparison between experiment and theory the extrinsic contributions to $\Delta F_M$ have also to be taken into account.

IV. RESULTS AND DISCUSSION

In the following, the experimental data obtained for the $(Ga,Mn)As$ samples under study are discussed.

A. Lattice parameters and strain

In order to study the structural properties of the $(Ga,Mn)As$/$\text{(In,Ga)}As$/GaAs samples, reciprocal space maps (RSM) of the asymmetric (224), (224), (224), and (224) reflections were recorded using HRXRD. Figure 2 exemplarily shows an RSM contour plot of the (224) reflection for a nearly unstrained $(Ga,Mn)As$ layer $(\varepsilon_{zz} = -0.04\%)$ grown on relaxed $(In,Ga)As$/GaAs template. $h$ and $l$ are the coordinates in $k$-space in units of the reciprocal lattice vectors along $[100]$ and $[001]$ in the GaAs substrate, respectively. $\Delta h$ and $\Delta l$ denote the shift of the peak position relative to that of the substrate. In the plot, $\Delta h$ and $\Delta l$ are only depicted for the $(Ga,Mn)As$ layer.

FIG. 2: Reciprocal space map around the asymmetric (224) reflections of a nearly unstrained $(Ga,Mn)As$ layer $(\varepsilon_{zz} = -0.04\%)$ grown on relaxed $(In,Ga)As$/GaAs template. $h$ and $l$ are the coordinates in $k$-space in units of the reciprocal lattice vectors along $[100]$ and $[001]$ in the GaAs substrate, respectively. $\Delta h$ and $\Delta l$ denote the shift of the peak position relative to that of the substrate. In the plot, $\Delta h$ and $\Delta l$ are only depicted for the $(Ga,Mn)As$ layer.

The relaxed lattice parameter $a_{rel}$ of a biaxially strained layer on (001)-oriented substrate is obtained relaxation in the buffer layer $(a_{||} > a_s)$. The lattice parameters $a_{||}$ of the $(In,Ga)As$ templates in the as-grown and annealed samples are plotted against the In content in Fig. 3(a). Apparently, post-growth annealing had no significant influence on $a_{||}$, which linearly increases with the In content.

For both $(Ga,Mn)As$ and $(In,Ga)As$, the HRXRD measurements yielded different values of $(h,l)$ for the (224) and (224) reflections, revealing a tilt of the lattice towards the [110] direction. The tilt of the $(Ga,Mn)As$ layer originates from an equal tilt in the $(In,Ga)As$ buffer pointing to an anisotropic relaxation of the $(In,Ga)As$ templates, typically found in layers grown on vicinal substrates. The samples under investigation, however, were grown on non-miscut (001) wafers. As can be seen in Fig. 3(b), the measured tilt angles tend to higher values with increasing In fraction. It should be emphasized that it is imperative to take the tilt into account when determining the lattice parameters in order to avoid erroneous results. This can be done by inserting into Eq. (11) the averaged values of the peak positions and shifts obtained from the (224) and (224) reflections. For the angle-dependent magnetotransport measurements, the influence of the tilt is negligible since the tilt angles observed are smaller than 0.06 degree.

The relaxed lattice parameter $a_{rel}$ of a biaxially strained layer on (001)-oriented substrate is obtained
from the relation

\[ a_{\text{rel}} = \frac{2C_{12}}{C_{11} + 2C_{12}}a_{\parallel} + \frac{C_{11}}{C_{11} + 2C_{12}}a_{\perp}, \]  

where \( C_{11} \) and \( C_{12} \) are elastic stiffness constants. As an approximation, we use the values \( C_{11} = 11.90 \times 10^{10} \) Pa and \( C_{12} = 5.34 \times 10^{10} \) Pa of GaAs for both the (Ga,Mn)As and the (In,Ga)As layers. In Fig. 4(a), \( a_{\text{rel}} \) is shown for the (Ga,Mn)As layers as a function of the In content in the (In,Ga)As buffer. It is found to be nearly unaffected by the (In,Ga)As template underneath. The fluctuations in the values of \( a_{\text{rel}} \) are mainly attributed to slight variations of the growth temperature. For all (In,Ga)As templates under study, the degree of relaxation defined by \( R = (a_{\parallel} - a_{\perp})/(a_{\text{rel}} - a_{\perp}) \) was observed to be above 80%. Once the vertical and relaxed lattice parameters of the (Ga,Mn)As layers are known, the vertical strain \( \varepsilon_{zz} \) can be calculated from the relation

\[ \varepsilon_{zz} = (a_{\perp} - a_{\text{rel}})/a_{\text{rel}}. \]  

In Fig. 4(b), \( \varepsilon_{zz} \) is plotted against the In content. The slight decrease of \( a_{\text{rel}} \) and \( \varepsilon_{zz} \) upon annealing is supposed to arise from the outdiffusion and/or rearrangement of the highly mobile Mn.

**B. Hole density and Curie temperature**

Determination of the hole concentrations \( p \) in (Ga,Mn)As is complicated by a dominant anomalous contribution to the Hall effect proportional to the normal component of the magnetization \( M \) (anomalous Hall effect). To overcome this problem, magnetotransport measurements were performed at high magnetic fields up to 14.5 T. Assuming the magnetization to be saturated perpendicular to the layer plane at magnetic fields \( \mu_0 H \geq 4 \) T, the measured transverse resistivity was fitted using the equation

\[ \rho_{\text{trans}}(H) = R_0 \mu_0 H + c_1 \rho_{\text{long}}(H) + C_2 \rho_{\text{long}}^2(H) \]  

for the ordinary and anomalous Hall effect with \( R_0, c_1, \) and \( c_2 \) as fit parameters. Here \( R_0 = 1/e^2p \) is the ordinary Hall coefficient and \( \rho_{\text{long}} \) the measured field-dependent longitudinal resistivity. The second term on the right-hand side arises from skew scattering and the third term from side jump scattering and/or Berry phase effects. As mentioned in Sec. II, the Curie temperatures \( T_C \) were inferred from the peak positions of the temperature-dependent resistivities \( \rho_{\text{long}} \). Considering that the \( T_C \) values thus obtained generally differ from those determined by temperature-dependent magnetization measurements, we estimate an error margin of up to 20%. Similar to \( a_{\text{rel}} \), neither \( p \) nor \( T_C \) are significantly influenced by the strain as shown in Figure 5. The values scatter around \( p_{\text{eng}} = 3.5 \times 10^{29} \) cm\(^{-3}\) and \( T_C = 65 \) K for the as-grown samples and \( p_{\text{ann}} = 5.8 \times 10^{29} \) cm\(^{-3}\) and \( T_C = 91 \) K for the annealed samples. It is well known that the lattice constant, the hole density, and the Curie temperature strongly depend on the concentration of Mn acceptors, MnI, MnII, double donors, and other compensating defects such as As\(_{Ga}\) antisites. The insensitivity of \( a_{\text{rel}} \), \( p \), and \( T_C \) to strain in the as-grown and annealed samples under study suggests the assumption that strain has no significant influence on the incorporation of MnGa, MnI,
and As$_{Ga}$. At least the sum of the changes caused by the different constituents seems to be unaltered. Moreover, the insensitivity of $T_C$ with respect to $\varepsilon_{zz}$ supports theoretical predictions that the magnetic coupling should be unaffected by strain, since the corresponding deformation energies are expected to be too small to significantly enhance or reduce the p-d kinetic exchange interaction.

C. Anisotropy parameters

Experimental values for the anisotropy parameters $B_{001}=B_{2\perp}+B_3$, $B_{3\parallel}$, and $B_{110}$ were determined by means of angle-dependent magnetotransport measurements. A detailed description of the corresponding procedure is given in the Refs. 21 and 22. It can be briefly summarized as follows. The longitudinal and transverse resistivities $\rho_{\text{long}}$ and $\rho_{\text{trans}}$, respectively, are measured as a function of the magnetic field orientation at fixed field strengths of $\mu_0H=0.11$, 0.26, and 0.65 T. At each field strength, $H$ is rotated within three different crystallographic planes perpendicular to the directions $n$, $j$, and $t$, respectively. The corresponding configurations, labeled I, II, and III, are shown in Fig. 6. The vectors form a right-handed coordinate system, where $j$ defines the current direction, $n$ the surface normal, and $t$ the transverse direction. For current directions $j \parallel [100]$ and $j \parallel [110]$, the resistivities can be written as:

$$\rho_{\text{long}} = \rho_0 + \rho_1 m_j^2 + \rho_2 m_n^2 + \rho_3 m_j^4 + \rho_4 m_n + \rho_5 m_j^2 m_n^2,$$

$$\rho_{\text{trans}} = \rho_6 m_n + \rho_7 m_j m_t + \rho_8 m_n^3 + \rho_9 m_j m_n^2,$$

where $m_j$, $m_n$, and $m_t$ denote the components of $m$ along $j$, $t$, and $n$, respectively. At sufficiently high magnetic fields, the Zeeman energy in $G_M(m)$ dominates and the magnetization direction $m$ follows the orientation $h$ of the external field. The resistivity parameters $\rho_i (i=1,...,9)$ are then obtained from a fit of the Eqs. (15) and (16) to the experimental data recorded at 0.65 T. With decreasing field strength, the influence of the MA increases and $m$ more and more deviates from $h$. Controlled by the magnetic anisotropy parameters, the shape of the measured resistivity curves changes and $B_{001}$, $B_{3\parallel}$, and $B_{110}$ are obtained from a fit to the data recorded at $\mu_0H=0.26$ and 0.11 T. In the fit procedure, $m$ is calculated for every given magnetic field $H$ by numerically minimizing $G_M$ with respect to $m$. Figure 6 exemplarily shows the angular dependence of $\rho_{\text{long}}$ and $\rho_{\text{trans}}$ for a nearly unstrained (Ga,Mn)As layer ($\varepsilon_{zz}=-0.04\%$) with $H$ rotated in the (001) plane (configuration I) and $j \parallel [100]$. The experimental data are depicted by red solid circles and the fits by black solid lines.

Applying the procedure described above to the whole set of (Ga,Mn)As layers under study, the resistivity parameters $\rho_i (i=1,...,9)$ and the anisotropy parameters $B_{001}=B_{2\perp}+B_3$, $B_{3\parallel}$, and $B_{110}$ were determined as functions of the vertical strain $\varepsilon_{zz}$. The results for the resistivity parameters were extensively discussed in Ref. 22. In the present work, we exclusively focus on the anisotropy parameters.

Figure 6(a) shows the values of the parameter $B_{001}=B_{2\perp}+B_3$ describing the uniaxial out-of-plane anisotropy. For both the as-grown and the annealed samples, a pronounced linear dependence on $\varepsilon_{zz}$ is found in qualitative agreement with the microscopic model calculations presented in Fig. 4(c). For zero strain, the cubic symmetry requires $B_{2\perp}=0$ and the extrinsic parameter $B_3\approx60$ mT is inferred from the intersections between the regression lines (dotted lines) and the vertical axis. If shape anisotropy was the only extrinsic contribution to the $m_j^2$ term of $F_M$, as assumed in Sec. III A, the value $B_3\approx60$ mT would correspond to a sample magnetization of $\mu_0M=2B_3\approx120$ mT. This value, however, exceeds the saturation magnetization determined by SQUID measurements by a factor of ~3. Figure 5 shows as an example the SQUID curves obtained for the as-grown and annealed samples with $\varepsilon_{zz}=0.2\%$. At the moment, the reason for this discrepancy is not yet understood. We suspect, however, that it might be related to the vertical gradient in the MA mentioned at the end of Sec. III. Assuming the value of $B_3$ to be nearly the same for all samples
under consideration, the strain-dependent intrinsic parameter $B_{2\perp}$ is obtained by subtracting $B_d$ from the measured $B_{001}$ data. In Fig. 8(b), the values of $B_{2\perp}$ derived in this way are shown together with model calculations performed within the microscopic theory (see Sec. IIIB). Using for $p$ the mean values $p_{\text{ag}}=3.5\times10^{20}$ cm$^{-3}$ and $p_{\text{ann}}=5.8\times10^{20}$ cm$^{-3}$ (see Sec. IVB), the calculated values of $B_{2\perp}$ are found to be in qualitative agreement with the experimental data if $B_G=-23$ meV is chosen for the as-grown samples and $B_G=-39$ meV for the annealed samples. The corresponding curves are depicted by the solid and dashed lines in Fig. 8(b). Comparing the exchange-splitting parameters with the respective hole densities, we find

$$
\frac{B_{G,\text{ann}}}{B_{G,\text{ag}}} \approx \frac{p_{\text{ann}}}{p_{\text{ag}}} \approx 1.7.
$$

(17)

For the annealed samples, theoretical results are also shown for $-32$ meV and $-23$ meV, demonstrating that the slope of $B_{2\perp}(\varepsilon_{zz})$ is drastically reduced with decreasing $B_G$. Remarkably, normalization of the experimentally derived values of $B_{2\perp}$ to the corresponding hole concentration $p$ yields the same linear dependence of $B_{2\perp}/p$ on $\varepsilon_{zz}$ for both the as-grown and the annealed samples as shown in Fig. 8(c). We thus find, at least for the range of hole densities and strain under consideration, the experimental relationship

$$
B_{2\perp} = K p \varepsilon_{zz},
$$

(18)

with $K=1.57\times10^{-19}$ T cm$^3$. If we assume a linear relation $B_G=A_F\beta M/6g\mu_B \propto p$, in accordance with Eq. (17), Eq. (18) can be reproduced by the microscopic theory. Note however, that this is not trivial, since $\Delta F_{M,\text{int}}$ explicitly depends on both $B_G$ and $p$. Anyhow, the relation
$B_4 \propto p$ demands a future detailed investigation.

The experimental values of the fourth-order parameters $B_4$ and $B_{12}$ are presented in Figs. 10(a) and 10(b), respectively. Whereas $B_4$ only slightly varies between $\sim -40$ and $-10$ mT, $B_{12}$ exhibits positive values close to 10 mT for $\varepsilon_{zz} \lesssim -0.15\%$ and negative values of about $-20$ mT for $\varepsilon_{zz} \gtrsim -0.15\%$. The lines depicted in Fig. 10 were calculated using the same values for $p$ and $B_G$ as in Fig. 8(b). Obviously, the change of sign of $B_{12}$ does not appear in the theoretical curves. Apart from this disagreement, the experimental data of the as-grown samples are again well reproduced for $B_G = -23$ meV. In the case of the annealed samples, now the splitting parameter $B_G = -32$ meV yields a much better description of the measured data than $B_G = -39$ meV, found to fit the strain dependence of $B_{11}$.

In view of the perfect quantitative interpretation of $B_{11}$ by the mean-field Zener model, this small discrepancy and the fact that the change of sign of $B_{12}$ is not reproduced by the calculations, should not be overestimated. The experimentally observed change of sign of $B_{12}$ may be caused by extrinsic influences, not accessible by the model, such as the increasing density of threading dislocations in the (Ga,Mn)As/(In,Ga)As layers with increasing In concentration. Moreover, we cannot rule out that the change of sign is an artifact of the experimental method for determining the relatively small anisotropy parameter $B_{12}$. The same problem has also been reported in Ref. 19, where the authors did not extract information on the fourth-order out-of-plane anisotropy parameters from their ferromagnetic resonance measurements, since the corresponding contributions to the MA were masked by the much larger contributions of the second-order out-of-plane term. As to the differing values of $-39$ meV and $-32$ meV for $B_G$ in the case of the annealed samples, it should be pointed out that for high hole densities the Fermi energy shifts deep into the valence band. Therefore, the values of the free energy obtained by using a $6 \times 6 \mathbf{k} \cdot \mathbf{p}$ effective Hamiltonian become increasingly unreliable when analyzing higher order contributions to the free energy. One should not jump to the conclusion that this has to be interpreted as a deficiency of the Zener model itself.

In agreement with the data presented in Refs. 19, 41, and 42, the experimental values of the extrinsic uniaxial in-plane parameter $B_{110}$ are much smaller than those of the cubic in-plane parameter $B_{44}$ at 4.2 K. As shown in Fig. 11, they scatter around zero with $-10 \text{ mT} \leq B_{110} \leq 10 \text{ mT}$.
Due to the strong dependence of $B_{001}$ on $\varepsilon_{zz}$, the out-of-plane axis [001] becomes magnetically harder with $\varepsilon_{zz}$ increasing from $-0.4\%$ to $0.2\%$. Neglecting the small influence of $B_{110}$ in our samples at 4.2 K, the critical strain $\varepsilon_{zz}^{\text{crit}}$, where a reorientation of the easy axis from out-of-plane to in-plane occurs, can be estimated from the condition $B_{001}+B_{4\perp}=B_{4\parallel}$. We obtain for the as-grown (Ga,Mn)As layers under study $\varepsilon_{zz}^{\text{crit}}=-0.13\%$ and for the annealed layers $\varepsilon_{zz}^{\text{crit}}=-0.07\%$. Remarkably, these values are very close to the $\varepsilon_{zz}$ values in Fig. 10 where $B_{4\perp}$ changes sign.

Since the MA sensitively depends on the individual growth conditions, care has to be taken when comparing the values of anisotropy parameters published by different groups. Keeping this restriction in mind, the data presented in this work are in reasonable agreement, e.g., with the results obtained by Liu et al. for a representative pair of compressively and tensily strained (Ga,Mn)As samples with 3\% Mn.

### D. Magnetostriction constant

Changing the magnetization of a ferromagnet, e.g. by an external magnetic field, leads to a variation of its geometrical shape. For crystals with cubic symmetry, the influence of an external magnetic field, leads to a variation of its geometrical shape. For crystals with cubic symmetry, the growth conditions, care has to be taken when comparing the values of anisotropy parameters published by different groups. Keeping this restriction in mind, the data presented in this work are in reasonable agreement, e.g., with the results obtained by Liu et al. for a representative pair of compressively and tensily strained (Ga,Mn)As samples with 3\% Mn.

#### V. SUMMARY

A series of (Ga,Mn)As layers with 5\% Mn was grown on relaxed graded (In,Ga)As/GaAs templates with In contents up to 12\%. In this way, the vertical strain $\varepsilon_{zz}$ in the (Ga,Mn)As layers could be gradually varied over a wide range from $-0.38\%$ (tensile strain) to $0.22\%$ (compressive strain). The strain was found to have no significant influence on the hole concentration, the Curie temperature, and the relaxed lattice parameter. Angle-dependent magnetotransport measurements were performed to determine the uniaxial and cubic anisotropy parameters. $B_{2\perp}$ turned out to be proportional to both the strain and the hole concentration. From this linear dependence, the magnetostriction constant $\lambda_{100}$ was determined. While $B_{2\parallel}$ and $B_{4\parallel}$ are nearly strain independent, $B_{4\perp}$ changes sign when the magnetic easy axis flips from in-plane to out-of-plane.

Microscopic calculations of the free-energy density were performed based on the mean-field Zener model of Dietl et al. They justify the approximations made in the parameterization of the free energy by considering only terms up to the fourth order. The strain-dependent anisotropy parameters derived from the calculations were found to be in good quantitative agreement with the experimental results. In the case of the as-grown samples, the values of $B_{2\perp}$ and $B_{4\perp}$ are even perfectly reproduced. The quantitative comparison between the comprehensive set of experimental data and the microscopic calculations may be considered a valuable contribution to the ongoing controversy on impurity band versus valence band in (Ga,Mn)As.

Using the orientation of the magnetization as the basic information bit of a non-volatile memory, the tailoring and manipulation of the MA is of special importance. As shown in this work, the choice of an appropriate (In,Ga)As template allows for an adjustment of $\varepsilon_{zz}$ close to the critical value $\varepsilon_{zz}^{\text{crit}}$. Then, the magnetization direction can be switched from in-plane to out-of-plane or vice versa, e.g., by minute variation of the piezo stress in a piezoelectric actuator/(Ga,Mn)As hybrid structure.

**Acknowledgments**

This work was supported by the Deutsche Forschungsgemeinschaft under Contract No. Li 988/4.

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