Irreversibility Line in Nb/CuMn Multilayers with a Regular Array of Antidots

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The transport properties of Nb/CuMn multilayers with a regular array of electron beam lithography obtained antidots have been measured at different temperatures in the presence of external perpendicular magnetic fields. Hysteretical plots have been measured at different temperatures in the presence of an irreversibility line. We discuss several possible mechanisms to clarify the nature of this line. Among them the most plausible seems to be the vortex melting mainly induced by quantum fluctuations.

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I. INTRODUCTION

The task of increasing the critical current density $J_c$ in superconducting materials has always been a widely studied subject [1], gaining even more interest after the discovery of high temperature superconductors (HTS) [2]. These studies are strictly related to the knowledge of the flux line pinning mechanism and to the reduction of the vortex mobility. Introducing artificial defects in superconducting materials as, for example, non-superconducting distributed phases [3], columnar tracks of amorphous material obtained by high energy ions [4] or geometrical constrictions such as channels or dots [5,6], is a very useful tool for a better understanding of the vortex dynamics and for obtaining higher $J_c$ values. The recent developments of the submicrometer electron beam lithographic techniques have made possible to reduce the typical size of these geometrical constrictions to values much smaller than the period of the vortex lattice, and comparable to those of typical superconducting coherence lengths [5,7]. Many experiments, performed on systems with such a regular array of defects [8] and several numerical simulations [9], have been focused on the study of the vortex properties at low magnetic fields close to the matching fields $H_n = n_p \Phi_0$ (here $n_p$ is the pins concentration and $\Phi_0$ is the flux quantum).

Other studies, performed at higher magnetic fields, have been related to the analysis of the vortex lattice shear stress in superconducting layered systems with the presence of artificially obtained weak pinning channels embedded in a strong pinning environment [6,8,10]. Due to the possibility of varying in a controlled way many different parameters such as the density, the dimensionality and the nature of the pinning centers [11], the study of the vortex dynamics in artificially layered conventional superconductors with the simultaneous presence of a regular array of pinning centers perpendicular to the layers is of great interest. Moreover, the natural layered structure of HTS allows to use these artificial systems as a model to help in discriminating among intrinsic and dimensional effects in the transport properties of HTS compounds [12].

In this paper we report on current-voltage ($I-V$) characteristics and resistance versus temperature, $R(T,H)$, measurements, in perpendicular external magnetic fields $H$, performed on two different series of Nb/CuMn multilayers with a square array of antidots. The choice of a superconducting (Nb)/spin glass (CuMn) layered system could be interesting particularly in view of the use as a model of HTS compounds. The two series have antidots with the same diameter, $D \approx 1 \mu m$, and different lattice distances between the antidots: $d \approx 2 \mu m$ in one series and $d \approx 1.6 \mu m$ in the other. The experiments have been performed on different samples having different anisotropies for each series. The $I-V$ curves measured at different temperatures and at different values of $H$ have shown, in regions of the $H-T$ phase diagram depending on the anisotropy of the system, a hysteretic behavior with sudden voltage jumps, which disappears approaching the critical field $H_{c2}(T)$ curve. From the analysis of the curvature of the logarithmic $I-V$ characteristics and from the study of the shape of the Arrhenius plots of the resistive transition curves, we have been able to relate the disappearing of such a hysteretic behavior to the presence of an irreversibility line (IL). We have discussed different possible mechanisms responsible for this IL. Among them the most plausible for our samples seems to be the vortex melting mainly induced by quantum fluctuations [19].
Regular arrays of antidots have been fabricated using Electron Beam Lithography to pattern the resist on a 2 inch Si (100) wafer. The Nb and CuMn layers were deposited by a dual-source magnetically enhanced dc triode sputtering system with a movable substrate holder onto the patterned resist and the final structures were obtained by the lift-off technique. Single antidots have a circular geometry and the antidot array is arranged in a square lattice configuration, see figure 1. The total area covered by the array is a square of $200 \times 200 \mu m^2$ with four separate contact pads connected to the vertices. Eight replicas of this structure are present on the same Si wafer to allow the fabrication of a series of multilayered samples with the same Nb thickness and variable CuMn thicknesses in only one deposition run [20]. The resist used is UV III from Shipley: UV III is a chemically amplified photosresist for the deep-UV range, but is widely used as an e-beam resist because it provides a good trade-off between reasonable sensitivity and high resolution. In our case it has been used as a positive resist, that is, the resist is retained where unexposed. A resist film thickness of 5800 Å has been obtained spinning the wafer at 1800 rpm. The resist has been exposed using a Leica Cambridge EBIMF 10 system operated at 50 kV. Several tests have been carried out in order to achieve structure profiles most suitable for lift-off. In particular the desired profile is that showing a moderate undercut. Also, developing times and post-exposure treatment have been optimized for profile improvement. After developing and post-baking at 130 °C the samples underwent RIE in $O_2$ for 30 s at 25 W rf power and 14 Pa oxygen pressure, in order to completely remove residual resist in the exposed areas. This treatment lowered the resist thickness to about 5000 Å. Fig.1 shows a Scanning Electron Microscope (SEM) image of the typical result of the fabrication process: in this case the antidots nominal diameter is 1 µm and the nominal period of the structure is 2 µm.

The number of bilayers of Nb and CuMn is always equal to six. The first layer is CuMn, the last one is Nb. The Nb nominal thickness, $d_{Nb}$, is 250 Å for all the samples in both the series. The CuMn thickness, $d_{CuMn}$, has been varied from 7 Å to 25 Å in one series ($d \approx 2 \mu m$) and from 4 Å to 20 Å in the other ($d \approx 1.6 \mu m$). The Mn percentage is always equal to 2.7. For reference a Nb/CuMn multilayer with $d_{CuMn}=13 \AA$ (Mn % =2.7) without antidots, but with the same configuration ($200 \times 200 \mu m^2$ square and four pads connected to the vertices), has been fabricated. The samples parameters are summarized in Table I. I – V characteristics have been registered at $T \leq 4.2$ K using a dc pulse technique. The temperature stabilization, during the acquisition of curves in the helium bath, was better than $10^{-3}$ K. The magnetic field was obtained by a superconducting Nb-Ti solenoid. From the measured temperature dependencies of the perpendicular and parallel upper critical field $H_{c2}$ (obtained at half of the resistive transitions $R(T, H)$) we deduced the values for the parallel and the perpendicular coherence length at zero temperature, $\xi_{\parallel}(0)$ and $\xi_{\perp}(0)$ respectively, and then the value of the anisotropic Ginzburg-Landau mass ratio $\gamma_0 = \xi_{\parallel}(0)/\xi_{\perp}(0)$ [21]. The different values of the critical temperatures for the samples of the two series having similar values of $d_{Nb}$ and $d_{CuMn}$ are probably related to the different Nb quality obtained in the two deposition runs.

Figure 3 shows $I – V$ curves for the sample NCMB at $T=2.60$ K for different applied magnetic fields in the range $0.03 < H < 0.70$ Tesla. At low magnetic fields the curves present hysteresis, not due to thermal effects, when registered both in forward and backward directions, i.e. increasing and decreasing the current [17]. Such hysteresis becomes smaller when $H$ is increased disappearing completely, in the limit of our experimental accuracy, when approaching $H_{c2}$. These features have been repeatedly obtained for the same sample in different measurements and are typical for all the samples of the two series with antidots. In figure 3b the $I – V$ characteristics for the sample NCMDA without antidots are always smooth and parabolic-like, typical of a type II superconductor.

In figure 4 we plot the $I – V$ curves in double logarithmic scale for the sample RNMC at $T=2.96$ K for different values of the magnetic field. A change in the curvature of the logV-logI curves clearly occurs at low voltages; this is usually related to the presence of an IL in the $H-T$ phase diagram [22], given by the points at which the logV-logI curve is linear. In all the samples measured, these points are always very close to the points at which the hysteresis in the $I – V$ curves disappears. As an example, in the figures 4a,b,c, are shown the $H-T$ phase diagrams for the samples NCMB, NCMD and NCMH, respectively. Circles distinguish the two dif-

| Sample | $d_{Nb}$ (Å) | $d_{CuMn}$ (Å) | $\rho_N$ (Ω cm) | $\rho_{Nb}$ (Ω cm) | $\rho_{CuMn}$ (Ω cm) | $\rho_{average}$ (Ω cm) |
|--------|--------------|----------------|-----------------|------------------|----------------------|-------------------------|
| NCMB   | 7            | 2.38           | 0.01            | 0.02             | 0.00                 | 0.01                    |
| NCMDA  | 10           | 2.38           | 0.01            | 0.02             | 0.00                 | 0.01                    |
| NCMDA  | 15           | 2.38           | 0.01            | 0.02             | 0.00                 | 0.01                    |
| NCMB   | 20           | 2.38           | 0.01            | 0.02             | 0.00                 | 0.01                    |
| NCMB   | 25           | 2.38           | 0.01            | 0.02             | 0.00                 | 0.01                    |
| RNMC   | 4            | 2.38           | 0.01            | 0.02             | 0.00                 | 0.01                    |
| RNMC   | 8            | 2.38           | 0.01            | 0.02             | 0.00                 | 0.01                    |
| RNMB   | 12           | 2.38           | 0.01            | 0.02             | 0.00                 | 0.01                    |
| RNMB   | 16           | 2.38           | 0.01            | 0.02             | 0.00                 | 0.01                    |

Table I. Some of the relevant sample features. $\rho_N$ is the resistivity at $T=10$ K. See the text for the meaning of the other quantities.
FIG. 1. Scanning Electron Microscope picture of a Nb/CuMn sample with a square lattice of antidots ($D \approx 1 \, \mu m$ and $d \approx 2 \, \mu m$).

FIG. 2. (a) Current-Voltage characteristics for the multi-layer NCMF at $T = 2.60 \, K$ for different magnetic field values. The increasing values are: 0.03; 0.06; 0.15; 0.55; 0.70 T. (b) Current-Voltage characteristics for the multilayer NCMD at $H = 0.03 \, T$ for different temperatures. The increasing values are: 2.30; 2.34; 2.60; 2.80; 2.91 K.

FIG. 3. Logarithmic Current-Voltage characteristics for the sample RNCMC at $T = 2.96 \, K$ for magnetic fields, increasing counterclockwise, of 0.20; 0.40; 0.80; 0.90; 1.10; 1.30; 1.50; 1.60; 1.70; 1.75; 1.80; 1.85; 1.95; 2.10 T. The numbers indicate some values of the magnetic field. The melting field is estimated to be equal to 1.75 T.

Different regimes of the vortex dynamics as determined from the disappearance of the hysteresis in the $I-V$ curves; up triangles indicate points where change in the curvature of the logV-logI occurs; squares correspond to the values of the perpendicular critical magnetic field. It is then evident that the change in the hysteretical behavior of the $I-V$ characteristics, is related to the IL as defined by the change in the logV-logI curvature. It is also interesting to note that the position of the IL in the $H-T$ plane moves away from the $H_{c2}$ line as the anisotropy of the samples increases.

Another way to determine the presence of an IL in the $H-T$ phase diagram of a superconductor is the study of the Arrhenius plot of the resistance versus the temperature curves [18]. In figure 5 the Arrhenius plot of the transition curves, recorded using a bias current of 2 mA, of the sample RNCMA is shown at different perpendicular magnetic fields. A well defined field dependent temperature $T^*$ separates two zones with very different activation energies. In particular, at $T < T^*$ a sudden increase in the Arrhenius slope signals a transition in the transport properties of the sample which can be related to the presence of the IL. In figure 6 it is shown the measured $H-T$ phase diagram for the sample RNCMC. The solid squares correspond to the perpendicular magnetic fields; the open squares correspond to the points in the $H-T$ plane at which the onset of hysteresis in the $I-V$ curves takes place, the open diamonds are defined taking into account the change of curvature of the logI-logV curves, and the open circles and up triangles are the points at which the slope in the Arrhenius plot of the transition curves, taken respectively at a bias currents of 2 mA and 6 mA, change as viewed in figure 5. It is evident that also in this case all the points (open symbols) fall again on the same curve, which can be identified as an IL.
III. DISCUSSION

In all the measurements performed the bias current was applied in the plane of the film and perpendicular to the direction of the external magnetic field, see figure 1. In this configuration, the Lorentz force acting on the vortices, tends to move them along the channels in between the antidots. On the other hand, in the narrower zones between adjacent antidots, the current density is much higher than in the channels, so that we locally have weaker pinning centers in these parts of the sample. Therefore, we can look at our superconducting layered system as made of alternating zones of strong pinning (the channels along the direction of action of the Lorentz force in figure 1), and weak pinning (the narrower zones between adjacent antidots), similarly to other cases reported in the literature \[6,7,15,16\]. The value of the matching field in both the series is very small, $H_n \approx 5$ Oe and also $d \gg \xi(T)$, where $\xi(T)$ is the temperature dependent coherence length which in our multilayers has typical values of about 100 Å. Therefore, in the superconducting state it is possible to have a vortex lattice inside the channels between the antidots. The pinning of these interstitial vortices is determined mostly by the intrinsic properties of the superconducting materials \[10,23\].

To start the analysis of our data we have first to determine the dimensionality of the vortex lattice in our samples. At magnetic fields lower than a critical value $H_{cr} \approx 4\Phi_0/\gamma_0 s^2$, where $s$ is the interlayer distance between superconducting layers, the vortices in adjacent layers are strongly coupled and vortex lines behave as three dimensional (3D). For our samples $H_{cr} \approx 10^3$ T, well above any applied fields, and we can exclude the appearance of decoupling of the vortex lines in our layered systems \[24\].

On the other hand, when the shear modulus $c_{66}$ of a vortex lattice is much lower than the tilt modulus $c_{44}$, the system can behave bidimensionally. In principle, thermal fluctuations could cause tilt deformations in the vortex line. The critical thickness value $d_{cr}$ of a film beyond which thermal fluctuation induced tilt deformations become relevant is given by \[25\]

$$d_{cr} \approx \frac{4.4\xi}{\sqrt{h(1-h)}}$$  \hspace{1cm} (1)

where $h = H/H_{c2}$. In multilayers, however, the $d_{cr}$ value is reduced by a factor $\gamma_0^2/25$ \[25\] which for our samples gives, in the range of measured temperatures and magnetic fields, $d_{cr}^{\text{multi}} \approx 200 \div 300$ Å. Typical thickness for our samples are in the range 1500 ÷ 1700 Å. This means that the vortex lattice in our multilayers is in a strong 3D regime.

FIG. 4. $H$–$T$ phase diagram for the sample (a) NCMB, (b) NCMC and (c) NCMH. Squares correspond to $H_{c2}$, circles correspond to the disappearence of hysteresis in the $I$–$V$ curves, up triangles correspond to the change of the curvature in the log$V$–log$I$ curves. The solid lines are calculated according to the equation 3.
curvature in logV-logI

samples we never obtain linearity of the crossover from flux creep to flux flow occurs [26]. In our equation 3.

The solid line has been calculated according to the relation

curvature in logV-logI

The values of the initial slope in the plots. At lower temperatures, the dissipation in the system is mainly due to the vortices in the weak pinning regions, and this results in a lower value of the activation energies. When also these vortices experience the transition from liquid to solid at \( T = T^* \), the slope in the plots increases again [16].

One of the proposed interpretation of the nature of the IL relies upon a depinning mechanism in which a crossover from flux creep to flux flow occurs [26]. In our samples we never obtain linearity of the \( I - V \) curves neither at high voltage where a uniform flux flow should be present, nor at small currents, where thermally assisted flux flow (TAFF) [27] should take place. If we fit our data with the relation \( V \sim I^\alpha \) the fitting exponent is always very high (\( \alpha > 10 \)). Therefore we exclude the possibility of flux creep-flux flow crossover in the presence of a pinning strength distribution which could also be responsible for the curvature change of the \( I - V \) curves when plotted in double logarithmic scale [28].

The \( I - V \) curves shown in figure 2a and 2b are very similar to those obtained as a result of numerical simulations for a superconductor with periodic pinning close to the matching field [13,14]. Considering that we are very far from \( H_n \) we cannot apply the results of Ref. [13] to explain our \( I - V \) curves. Nevertheless, the main observed features indicate the presence of a region in the \( H - T \) plane where plastic vortex motion probably takes place. Below some crossover value \( H_{pl} \), vortices experience plastic motion which usually reveals in hysteretical curves [29]. Above \( H_{pl} \), \( I - V \) curves are smooth, hysteresis vanish and the vortex motion start to be a flow of vortex liquid [29]. The vortex melting scenario along with the simultaneous presence of weak and strong pinning channels, can also explain the observed Arrhenius plots. In fact, immediately below \( T_{onset} \) (defined as the temperature where the electrical resistance \( R \) is 0.9 of its value in the normal state), the solidification of the vortices in the strong pinning channels determines the high values of the initial slope in the plots. At lower temperatures, the dissipation in the system is mainly due to the vortices in the weak pinning regions, and this results in a lower value of the activation energies. When also these vortices experience the transition from liquid to solid at \( T = T^* \), the slope in the plots increases again [16].

Melting in the vortex lattice can be induced by thermal fluctuations [30]. The melting temperature at which the vortex lattice goes from a solid phase to a liquid one, can be obtained by using the 3D thermal melting criterion

\[
c_L \approx \frac{3G_i}{\pi^2} \frac{h}{(1-h)^3} \frac{t_m^2}{(1-c_t)}
\]

where \( c_L \) is the Lindemann number, \( T_c \) is the superconducting transition temperature (defined in our case at the point where the electrical resistance \( R \) of the sample becomes less than \( 10^{-4} \) \( \Omega \)), \( t_m = T_m/T_c \) is the reduced melting temperature, and \( G_i \) is the Ginzburg number which determines the contribution of the thermal fluctuations to the vortex melting given by \( G_i = (1/2)(2\pi \mu_0 k_B T_c \lambda_{||}(0)\gamma_{||}/\Phi_{0}^{2}\xi(0)) \), where \( \lambda_{||} \) is the in-plane penetration depth which, for all our samples, has been assumed to be equal to 1500 Å [31]. Melting usually occurs when \( c_L \approx \frac{1}{2} \). When we try to fit the IL observed in our samples with Eq.2 we get \( c_L \sim 10^{-4} \). This extremely low value for the Lindemann number makes unreasonable to consider the IL as due to 3D thermal melting.

However, as first pointed out by Blatter and Ivlev [14] in moderately anisotropic superconductors at low temperatures one could not exclude the contribution of quantum fluctuations to the melting. In this case the total fluctuation displacement of vortex line is \( \langle u >^2 = \langle u >^2_{th} + \langle u >^2_{q} \), where \( \sqrt{< u >^2_{th}} \) is the average dis-
placement due to thermal fluctuations and $\sqrt{\langle u^2 \rangle_q}$ is the average displacement due to quantum fluctuations. $\langle u^2 \rangle_q$ diminishes with the temperature, while $\langle u^2 \rangle_q$ does not depend on the temperature and at low values of $T$ one could expect $\langle u \rangle_q \approx 0$. The amplitude of $\langle u^2 \rangle_q$ depends on the ratio $Q^*/\sqrt{G_i^*}$ where $Q^* = e^2 \rho / h s$, with $h$ the Planck constant and $e$ the elementary charge. If $Q^*/\sqrt{G_i^*} \gg 1$, the contribution of quantum fluctuations is crucial. For the samples discussed here we always get $Q^*/\sqrt{G_i^*} > 30$ which justifies the possibility of an important contribution coming from quantum fluctuations [32]. In this case the melting line is given by [33]

$$h_m = \frac{4Q^2}{[1 + (1 + 4Q^2\Theta^2)]^{1/2}}$$

where $h_m = H_m/H_{c2}$, $t = T/T_c$ is the reduced temperature, $\Theta = \pi c^2_1(t^{-1} - 1)/\sqrt{G_i^*}$, $Q = Q^* \Omega / \pi \sqrt{G_i^*}$ with $\Omega$ a cut-off frequency generally of the order of the Debye frequency and $\tau$ an effective electronic relaxation time $(\hbar/k_B T_c \approx \tau)$ [33]. As we already showed before [34], the values of $\Omega$ and $\tau$ in Nb/CuMn are in the range $(2 \div 3) \times 10^{13}s^{-1}$ and $(1 \div 5) \times 10^{13}s$ respectively. Therefore, for all the samples studied we have assumed $\Omega = 3 \times 10^{13}s^{-1}$ and $\tau = 5 \times 10^{13}s$. In this way we reduce the number of free fit parameters in Eq.3 to only one, namely the Lindemann number $c_L$.

The solid line in Fig.6 has been calculated according to Eq.3 using for the Lindemann number a value of $c_L=0.23$. Also the solid lines in the Figures 4a, 4b and 4c have been calculated according to Eq.3. For the sample NCMC, Fig.4b, we obtain good agreement with the experimental data for $c_L = 0.19$, while for the sample NCMH, Fig.4c, the solid line is obtained taking $c_L = 0.09$. The agreement between experimental data and theoretical curves is very good for all the samples studied. The $c_L$ values, as shown in Table I, become smaller with increasing anisotropy reaching in the case of sample NCMH a value slightly below 0.1 [19]. When increasing the anisotropy of the system, the coupling between adjacent superconducting layers reduces and vortex lines become more soft. The influence of the thermal fluctuations on the vortex dynamics is strongly dependent on this coupling. Qualitatively, therefore, the reduction of the $c_L$ values with increasing anisotropy could be related to the change in the topology of the vortex system.

On the other hand, the softening of the vortex system could also determine a situation in which thermal fluctuations are able to cause tilt deformations. Anyway, if we try to fit the experimental points in figures [4a] and [4b] using the 2D pure thermal melting curve [33]

$$\alpha d H_{c2}(T) \approx \frac{(1 - 0.58h_m - 0.29h_m^2)(1 - h_m)^2}{\kappa^2 T(1.25 - 0.25t)} = 1$$

we do not obtain any agreement with the data. Here $\alpha = A \Phi_0 (1.07)^2/32\pi \mu_0 K_B$, $\kappa = \lambda ||/\xi_||$ and $d$ is the thickness of the sample. $A$ is a renormalization factor of the shear modulus $c_{66}$ due to non linear lattice vibrations and vortex lattice defects and is $A \approx 0.64$ [36].

![FIG. 7. Values of the activation energy in the zone 2 for a not-perforated sample (solid squares) and values of the activation energy in the zone 1 for a perforated sample (open squares). Insert: schematic of a typical Arrhenius plot observed in a perforated and a not-perforated Nb/CuMn multilayer together with the identification of the zones 1 and 2.](image-url)

We want to point out that the quantum melting theory has been successfully applied to describe the vortex behavior also in not-perforated Nb/CuMn multilayers [34]. In that case the melting line was determined by analyzing in Arrhenius fashion the measured $R(T)$ curves in perpendicular magnetic fields. The shapes of the Arrhenius plots, see for example figure [4a] in ref. [32], were very similar to those observed in the case of perforated samples, suggesting the presence of two types of pinning centers also in the case of non perforated samples. In not perforated samples, edge pinning could be relevant and obviously stronger than intrinsic pinning [31]. Therefore one could interpret the shape of the Arrhenius plots in not perforated Nb/CuMn multilayers as due to vortex transition from liquid to solid first of the vortices at the edges and then, at lower temperatures, of the vortices intrinsically pinned in the inner part of the samples. If this interpretation is correct, the slopes of the Arrhenius plots measured in not perforated samples in the zone 2 (see insert in figure [4a]) should be very close to the slope measured in the zone 1 in perforated samples. In fact, in both cases, this slope should be related to the activation energy of vortices intrinsically pinned inside the...
system. In figure 5 the solid points refer to the values of the activation energy in a typical not-perforated sample measured in zone 2, while the open symbols refer to the values of the activation energy in a perforated sample (RNCMA) measured in zone 1. The two samples have been chosen to have similar critical temperatures. Also the \( R(T, H) \) curves have been taken using a similar value for the bias current density \( J_b \). The quite nice agreement between the two sets of data supports our idea that, in both cases, they are a measure of the intrinsic pinning in the material.

The presence of the antidot array in the multilayers makes more easily measurable the vortex melting. In fact, in the case of perforated samples one is able to detect the change in the slope of the Arrhenius plots using low values of the bias current (\( \sim 100 \mu A \)) while for not perforated samples bias currents of \( \sim 1 m A \) are needed to observe the same effect (the IL in a superconductor does not depend on the value of the bias current). This is consistent with the idea that in antidoted samples the melting takes place in the zones with weaker pinning when compared to the case of not perforated samples in which the measured vortex phase transition takes place in the zones of intrinsic pinning. As a consequence of this also the hysteresis is much easier detectable in antidoted samples, in regions of the \( I - V \) characteristics not to close to the \( H_{c2}(T) \) curve.

The influence of the regular array of antidots on the vortex properties is also confirmed by the behavior in our samples of the vortex correlation length in the liquid phase \( \xi_+ \), defined as

\[
\xi_+ \approx \xi_{+0} \exp \left\{ b \left( \frac{T_m}{T - T_m} \right)^\nu \right\} \tag{5}
\]

where \( b \) is a constant of the order of the unity, \( \nu = 0.36963 \) and \( \xi_{+0} \), being the smallest characteristic length scale in the liquid, is of the order of \( a_0 \), the vortex lattice parameter. According to the melting theory the shear viscosity \( \eta(T) \) of the vortex liquid starts to grow up approaching the liquid-solid line from above, when \( \eta \sim \xi_+^2(T) \).\[8] The curves of \( \xi_+ \) versus the temperature for different applied magnetic fields are reported in figure 5 for the sample NCMH. All the curves start to diverge when the value of \( \xi_+ \) becomes comparable to the average distance among the antidots, i.e. when \( \xi_+ \approx d = 1 \mu m \). Similar results have been obtained for all the samples investigated. This is exactly what we expect, if we look at the investigated system as a vortex ensemble constrained in the narrow channels among the lines of the antidots. In this case, in fact, the melting transition at \( H = H_m \) is going to be observed when the correlation length of the liquid \( \xi_+ \) reaches the value of the width of the channels. The results shown in figure 5 clearly indicate the influence of the antidots lattice on the vortex dynamics in our samples.

In conclusion, we have studied transport properties of superconducting (Nb)-spin glass (CuMn) multilayer with a regular array of antidots by measuring \( I - V \) curves in perpendicular magnetic fields. The measurements have been performed far above the matching conditions. The dynamic phase diagram has been drawn out from the analysis of these measurements. Two regions corresponding to plastic flux flow motion and to the motion of the vortex liquid have been distinguished. Melting occurs mostly due to quantum fluctuations and the presence of the antidots renders more easier to detect the melting due to the weaker pinning in the zones with higher local current density.

![FIG. 8. Dependence of the correlation length \( \xi_+ \) versus the temperature at different magnetic fields for the sample NCMH.](image)

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