Lethal Mutagenesis in Viruses and Bacteria

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In this work we study how mutations which change physical properties of cell proteins (stability) impact population survival and growth. We present a model in which the genotype is presented as a set folding free energies of cell proteins. Mutations occur upon replication, so stabilities of some proteins in daughter cells differ from those in the parent cell by amounts deduced from the distribution of mutational effects on protein stability. The genotype-phenotype relationship posits that the cell’s fitness (replication rate) is proportional to the concentration of its folded proteins, and that unstable essential proteins result in lethality. Simulations reveal that lethal mutagenesis occurs at a mutation rate close to 7 mutations in each replication of the genome for RNA viruses, and at about half that rate for DNA-based organisms, in accord with earlier predictions from analytical theory and experimental results. This number appears somewhat dependent on the number of genes in the organisms and the organism’s natural death rate. Further, our model reproduces the distribution of stabilities of natural proteins, in excellent agreement with experiment. We find that species with high mutation rates tend to have less stable proteins compared to species with low mutation rates.
INTRODUCTION

Mutation rates play an important role in the evolution and adaptation of bacteria and viruses. Considerable experimental evidence suggests that high mutation rates in RNA virus populations have powered their rapid evolution (DE LA TORRE et al. 1990; DOMINGO 2000; DOMINGO et al. 1978; EGGERS and TAMM 1965). However, artificially elevated mutation rates were shown to have deleterious effects on the fitness of RNA viruses, and eventually lead to extinction of the viral population beyond certain mutation rate thresholds (ANDERSON et al. 2004; BULL et al. 2007; FREISTADT et al. 2004; GRACI et al. 2007; GRACI et al. 2008; GRANDE-PEREZ et al. 2002; LOEB et al. 1999; PARIENTE et al. 2001; SIERRA et al. 2000; ZELDOVICH et al. 2007). This observation is called lethal mutagenesis for RNA viruses. Several authors proposed to use lethal mutagenesis to cure or control infection with RNA viruses, using certain mutagens (ANDERSON et al. 2004; FREISTADT et al. 2004). The possibility of lethal mutagenesis in bacteria was also suggested and studied recently (ANDRE and GODELLE 2006; BULL and WILKE 2008; GESSLER 1995).

Previously, many attempts have been made, using population genetics, to theoretically describe the effect of mutation rates on the survival of a population (GESSLER 1995; HAIGH 1978; MULLER 1964). The effect has frequently been described within the paradigm of Muller’s ratchet, (ANDERSSON and HUGHES 1996; HAIGH 1978; MULLER 1964) where the genome of an asexual organism accumulates stochastic deleterious mutations in an irreversible manner, leading to the systematic decrease in the fitness of the organism. The concept of Muller’s ratchet applies to finite, asexual
populations. It states that if back mutations cannot occur, eventually any finite asexual population will accumulate deleterious mutations and the mutation-free wild type genotype would be lost. While such models provided some useful insights into the phenomenon of lethal mutagenesis, they often assume a single fitness peak, absence of back or compensating mutations and depend heavily on arbitrary parameters, such as selection coefficients or the deleterious mutation rates. Such analyses therefore lack a more fundamental connection between the physical properties of the proteins within the organism, the metabolic network of the organism, and the feedback relationship between the mutation rate and organismal fitness.

In recent years, several theories of lethal mutagenesis have been proposed (Bull et al. 2007; Bull and Wilke 2008; Guo et al. 2004; Zeldovich et al. 2007). In a marked departure from earlier phenomenological approaches Zeldovich et al. (Zeldovich et al. 2007) suggested a model assuming that the loss of protein stability would lead to the loss of essential functions within the organism and therefore to lethal phenotype. The evolution of a population in this model was mapped to a diffusion process in a multidimensional hypercube where each dimension represented stability of proteins encoded by an essential gene and adsorbing boundary conditions at $\Delta G = 0$ boundaries (where $\Delta G$ is the difference between free energy of the folded and unfolded proteins which is the thermodynamic measure of protein stability (Zeldovich et al. 2007)) were imposed to account for the fact that loss of stability confers lethal phenotype on an organism. This model differs from previous approaches in that, instead of depending on arbitrarily calibrated parameters such as selection coefficients or deleterious mutation rates, it is based only on the statistical distribution of proteins’ folding free energy change.
after point mutations, which had been directly derived from in vitro experiments. Furthermore, it predicts a lethal mutagenesis threshold that is consistent with experimental findings and discovers a deep relation between fundamental biophysical properties of proteins, the mutation rate, and organismal fitness.

However, despite these insights, the model proposed by Zeldovich et al. (ZELDOVICH et al. 2007) is based on a number of simplifying assumptions. First, it assumes a uniform mutation supply within the population; meaning that at any time, mutations could occur in any organism in the population with an equal and constant probability. However, in real biological systems mutations are coupled to replication. While the formalism developed by Zeldovich et al. (ZELDOVICH et al. 2007) allows to consider the case when mutations are coupled to replication (see Methods in (ZELDOVICH et al. 2007)) this formalism gives numerically accurate predictions for the coupled mutation-replication only in the limit of low mutation rates. However lethal mutagenesis occurs when mutation rate is relatively high (approximately six mutations per genome per replication according to (CROTLY et al. 2001; ZELDOVICH et al. 2007)). Second, the model developed in (ZELDOVICH et al. 2007) assumes a very simple ‘’$\Theta$’’-function-like’’ fitness landscape whereby fitness is the same for all protein stabilities as long as proteins are stable, i.e. it is flat for all $\Delta G < 0$. However in reality as proteins become less stable they spend greater fraction of time in unfolded state reducing therefore the effective concentration of functional proteins, which may affect fitness. Our study overcomes these limitations in a new computational model as outlined below.

If the organism has conservative replication mechanism, as is the case for RNA viruses, then mutations would only occur, with certain probabilities, in the descendent
copy, while the parent copy would remain unchanged (that may also be the case in organisms with double-stranded genomes where methylation mechanism keeps master copy of the genome preserved). If the organism has semi-conservative replication, as in bacteria and DNA viruses and double-stranded RNA viruses, then mutations could happen with certain probabilities in both daughter organisms.

Here we present a detailed study of fitness effect of protein stability changing mutations, based on the coupled mutation-replication scenario and more explicit physical consideration of the effect of protein stability on fitness. Simulating evolution and population growth in this model we observe lethal mutagenesis in conservative and semi-conservative replicating populations. Further, we show how stationary distribution of protein stabilities (folding free energies) emerges and discuss the physical and evolutionary reasons for the observed moderate stability of proteins.

THE MODEL

In our model, we assume that the replication rate of an organism depends on the functionality of each of the proteins involved in the organismal replication process (below we will call such proteins rate determining proteins and genes encoding them rate determining genes). Rate determining genes do not necessarily constitute the whole genome. Instead, it could be a small or large subset of the genome, and the number may vary between species and strains (NISHIKAWA et al. 2008). However, an organism is only able to replicate efficiently when all of these proteins are able to function properly (COUNAGO et al. 2006). Failure of a single rate-determining protein might result in the organism’s dysfunction and hence reduce the organismal replication rate.
We also note that the subset of rate determining genes may be smaller than the subset of essential genes. The difference between the two is that essential genes (i.e. the ones whose knockout causes lethal phenotype) may not affect growth rate directly. In contrast, the supply of functional proteins which are encoded by rate determining genes may affect critically the ability of a cell to replicate. An example of such proteins could be enzymes involved in nucleotide and amino acid metabolism, DNA polymerases etc. Essential but not necessarily rate determining proteins may be enzymes which are involved in metabolism of certain nutrients, proteins responsible for motility under certain conditions etc.

Here we assume that the organism’s replication rate is directly related to the copy numbers of rate determining proteins in their folded, i.e. functional states. Protein domains are known to fold thermodynamically two-state (Privalov 1979; Privalov and Khechinashvili 1974; Shakhnovich and Finkelstein 1989) which means that only unfolded and folded forms of a protein domain can be present in an ensemble in significant quantities. The fraction of time a protein spends in its folded state is then given by

\[ f_i = \frac{e^{\frac{G_f^i}{kT}}}{e^{\frac{G_f^i}{kT}} + e^{\frac{G_u^i}{kT}}} = \frac{1}{1 + e^{\frac{\Delta G_i}{kT}}} \]  

(1)

where \( G_f^i \) and \( G_u^i \) are free energies of the folded and unfolded forms of protein \( i \) respectively and \( \Delta G_i = G_f^i - G_u^i \) is the difference between the two representing the
stability of protein $i$. Factors $f_i$ determine effective concentrations of functional rate determining proteins in the organism. For simplicity, we assume that the proteins regulating organism replication are independent of each other; therefore the percentage of folded proteins should be a function of only their stabilities $\Delta G_{f_i}^{\text{u}}$ and the environmental temperature.

The organismal fitness (growth rate in a fixed environment) is therefore determined by the percentage of properly folded rate determining proteins in the organism. The replication rate for an organism with $\Gamma$ different proteins controlling the replication process can be expressed as:

$$b = b_0 \prod_{i=1}^{\Gamma} f_i \quad (2)$$

here, $b_0$, is the overall birth rate, a constant parameter that is determined by other organismal environmental factors such as temperature, acidity, or nutrition and by expression levels of all rate determining genes (which are assumed constant in this model).

Eqs (1) and (2) establish the fitness landscape in our model. The key aspect of the model is that it keeps track of the coarse-grained quantity of evolving proteins, their stability, rather than their exact sequences (Bloom et al. 2007; Zeldovich et al. 2007). In the earlier work (Zeldovich et al. 2007) the fitness landscape had a strict step–function form where fitness (growth rate) was assumed to be constant when all essential proteins are stable ($\Delta G < 0$) and 0 when at least for one essential protein $\Delta G \geq 0$. Here fitness depends on protein stability in a more continuous fashion because in addition to the “step-function” death condition of (Zeldovich et al. 2007), in this model we
assume the effect of copy number of folded proteins on fitness. However, the dependence of fitness on stability is still a step function-like whereby it is more pronounced at low stabilities and plateaus at moderate stability as suggested by ‘Fermi-Dirac-like’ function of Eq.(1). According to Equation (1), as long as a rate-determining protein has folding free energy $\Delta G < -3 \text{kcal/mol}$, then more than 99% of this protein molecules are properly folded at room temperature, therefore further stabilization of this protein would not bring too much additional growth rate. On the other hand, the effect of copy number of folded proteins on fitness does impose a strong limitation on less stable proteins. For example, if three rate determining protein each have stability around -1kcal/mol, while all other proteins are more stable than -3kcal/mol, then the overall fitness is decreased by 40% compared to another organism whose all rate-determining proteins are more stable than -3kcal/mol.

Mutations change folding free energy of proteins. The magnitude of the change is treated as stochastic in our model, whereas experimental evidence (FERSHT 1999; KUMAR et al. 2006; ZELDOVICH et al. 2007) has shown that statistically the impact of mutations on protein stability is biased towards the deleterious side. The statistics of changes of proteins free energy after point mutations, $\Delta \Delta G$, has been analyzed in (KUMAR et al. 2006; ZELDOVICH et al. 2007). It is Gaussian-like with an average destabilizing effect of around 1kcal/mol, and standard deviation of around 1.7kcal/mol. Several authors discussed the possibility that the distribution of $\Delta \Delta G$ itself could depend on the stability of the wild-type protein (BLOOM et al. 2006; DEPRISTO et al. 2005). To address this issue we considered the thermodynamic data on over 2000 point mutations available in the database ProTherm (KUMAR et al. 2006) and did not observe a pronounced statistical dependence of thermodynamic effect of mutations on stability of wild-type proteins, (Figure 1).

The value of fixed death rate can be highly species-dependent. Although the possibility of bacteria aging has been explored, their natural death rate is small, and the aging process would take a long time (MENON et al. 2003; STEWART et al. 2005).
However, for viral particles, because of various lytic and non-lytic immune responses (Wodarz et al. 2002), their death rate can vary from a small fraction to the majority of the viral population being eliminated at each replication cycle. Therefore, in the following discussion, we will neglect natural death rate for bacteria and focus on the effect death rate for viruses, in agreement with previous viral lethal mutagenesis models (Bull et al. 2007). Unlike bacteria viruses replicate in bursts, involving several generations. Here, for simplicity, and in order to better compare with bacterial lethal mutagenesis analysis, we introduce a coarse-grained (in time) description of viral replication which includes effective per generation average death rate parameter. For example, for a viral particle with burst size \(~1000\) (occurring over \(\log_2 1000 \sim 10\) generations) and survival probability \(10\%\) after lysis, we assume that per generation death rate is \(D\) around \(20\%\) per generation. In other words, assuming the burst size is \(b\), and survival probability after the burst is \(S\), the per generation death rate parameter can be estimated as:

\[
(1 - D)^{\log_2 b} = S
\]

\[
D \sim (1 - S^{\log_2 b})
\]

This is a strong simplification that depends on the stability of various external biological factors. Nevertheless, assuming a constant death rate per unit time serves as a convenient parameter for comparing the lethal mutagenic processes across strains and species. The major assumptions of our model for different species are summarized in Table 1.

In addition to the replication and mutation factors, we also recognize from gene knockout experiments (Gerdes et al. 2003; Kobayashi et al. 2003), that the failure for any key protein to fold in a cell can be lethal to the organism. Therefore, we assume, as in
that loss of stability for any protein (in which case the folding free energy for this protein is greater than 0) causes the death of an organism (i.e., confers the lethal phenotype). In our analysis this biological requirement is cast as a boundary condition (Zeldovich et al. 2007):

\[ P(\Delta G_1, \Delta G_2, \ldots, \Delta G_{\Gamma}, t) = 0 \text{ if } G_i \geq 0 \quad i = 1, \ldots, \Gamma \] (3)

Here \( P \) is the number of organisms in the population which have genotype \( \{\Delta G\} = (\Delta G_1, \Delta G_2, \ldots, \Delta G_{\Gamma}) \) at time \( t \). We note that in our coarse-grained model, which does not explicitly treat protein sequences, the genotype of an organism is just the set of stabilities of its proteins.

The relation (3) indicates that there are no organisms in the population whose genomes encode unstable proteins (we focus here on viruses and bacteria which supposedly do not contain intrinsically disordered proteins (Xie et al. 2007)). The biological motivation for this condition is that not only expression of unstable proteins deprives the organism of functional proteins but also may lead to their aggregation causing the death of an organism (Drummond et al. 2005).

To summarize, we compare our model with several traditional population genetics models. Most population genetics models assume (explicitly or implicitly) a single fitness peak: wild-type genotype (i.e., literally the genome sequence) is most fit while any mutation confers selective disadvantage. Due to huge size of sequence space back mutations which restore original wt genotype are not allowed. Compared to traditional population genetics models, our fitness-mutation feedback function is more complicated. A detailed comparison between this model and other population genetics models is given.

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in Table 2. The key difference between them is that in our model the fitness landscape is considered in the coarse-grained space of protein stabilities rather than in the space of genomic sequences as in traditional approaches. The crucial point is that in our approach ‘’back mutations’’ are the ones which restore (or improve) protein stability rather than the ones which restore the original genome sequences. For that reason beneficial mutations are quite frequent in our model and some form of equilibrium between beneficial and deleterious mutations establishes as can be seen below.

Simulation of evolution of populations.

Based on these principles, we simulate the evolution of populations for the cases of semi-conservative and conservative replication. First, we prepare initial species with 100 identical organisms of the same genotype; initial stabilities of \( \Gamma \) proteins in each organism have random values drawn from the analytical distribution of the functional form described in our previous work (Zeldovich et al. 2007). At each time step an organism can replicate with probability determined by the genotype-dependent replication rate parameter given by Eq.2. An organism is eliminated as soon as a mutation occurs which confers any of its proteins a folding free energy value greater than zero.

Upon replication, mutations may happen in a descendant organism. Mutation in our model represents the change in stability of one or more proteins in the daughter organism compared with parent organism, i.e. genotype of the daughter organism can be presented as

\[
\{ \Delta \tilde{G} \}_{\text{daughter}} = \{ \Delta \tilde{G} \}_{\text{parent}} + \{ \Delta \Delta \tilde{G} \}
\]
where \( \{\Delta \Delta G\} = (\Delta \Delta G_{i_1}, \Delta \Delta G_{i_2}, \ldots, \Delta \Delta G_{i_s}) \) describes changes of stabilities upon a replication event which resulted in \( s \) mutations in proteins \((i_1, i_2, \ldots, i_s)\). For semi-conservative replication, mutations might occur in both the parent copy and the descendent copy. If it is conservative replication, mutations would then occur in the descendent copy only. We generate the number of mutations \( s \) at each replication in a daughter organism, according to a Poisson distribution, and the parameter of the Poisson distribution \( m_{\text{organism}} \) is the average number of mutations per genome per replication, for this particular species. The mutation rate per gene is then \( m_{\text{gene}} = m_{\text{organism}} / \Gamma \). After selecting \( s \) - the total number of proteins to be mutated at a given replication event - we decide which proteins to mutate by selecting the set \((i_1, i_2, \ldots, i_s)\) at random. When mutation occurs, we alter the protein stability by an amount drawn from the Gaussian distribution with mean 1kcal/m and standard deviation 1.7kcal/m derived from the statistical analysis of experimental data on effects of point mutations on protein stability (Kumar et al. 2006; Zeldovich et al. 2007). The mutant daughter organism will therefore have an altered fitness value (derived from (Eq. (2))), due to the changes in stability of some of its proteins.

For both bacteria and viruses, we impose an upper limit of population size of 5000 organisms by culling excess organisms at random. Throughout this study \( Nm >> 1 \) for both bacteria and viruses, since we focus primarily on the high mutation rate regime where lethal mutagenesis may occur.
We set a constant death rate for viruses. At each generation, depending on the death rate, we randomly kill a certain fraction of new organisms. Thus population dynamics in our simulations essentially maps into a peculiar $\Gamma$-dimensional diffusion process with branching and growth with “position-dependent” (Eq.2) branching rate and with proper absorbing boundary conditions as explained above (Eq.3). We ran multiple independent simulations to eliminate the effect of genetic drift. During simulations, we let organisms evolve in a stable environment for about 5000 generations, and we study the population dynamics and evolution of protein stabilities for a range of parameters.

RESULTS

Lethal Mutagenesis with Semi-conservative Replication (for Bacteria and DNA Viruses)

We define the lethal mutagenesis threshold as the minimum mutation rate that can result in a species with sufficient initial large population to eventually go extinct. As shown in Figure 2 as well as in previous work (ZELDOVICH et al. 2007), as long as the mutation rate is smaller than some critical value, the population can sustain itself for a sufficiently long time. However when mutation rate exceeds a certain threshold lethal mutagenesis occurs as can be seen in Figure 2.

The effect of mutations on population dynamics depends on the number of rate determining genes $\Gamma$ as shown in Figure 3. The lethal mutagenesis threshold shown in Fig.3B is slightly different numerically from that predicted in the previous analytical model (around 3 mutations per genome per replication for semi-conservative replication and around 6 for conservative one for all genome sizes)(ZELDOVICH et al. 2007), and the reasons may be two-fold. Firstly, herein we consider the coupled replication-mutation
scenario, in which mutations only occur during replication events. Secondly, we also consider a more realistic fitness landscape, in which the stabilities of proteins affect the organism replication rate; that is, all rate determining proteins have certain influence on the rate of replication. The more properly folded copies of a protein are there in the organism, the faster the replication rate and hence higher the organism fitness. Hence there is a collective contribution term from all rate determining genes in the organism. As shown in Figure 3A, at fixed mutation rate of 3 mutations per genome per replication, the increase in the number of rate determining genes results in a lower probability that the species will become extinct.

A possible reason for dependence of lethal mutagenesis threshold on the number of genes $\Gamma$ in the present model is as follows. Prior to lethality, organisms enter the regime where one or several proteins are marginally stable which causes considerable slowing down of their replication rate. Therefore, compared to a simple organism, a complicated organism with more rate determining genes is more likely to enter the slowly replicating phase, and deleterious mutations which finally cause death will accumulate slower in time. Hence higher genome sizes lead to some increase of the lethal mutagenesis threshold.

In order to check this assertion, a control simulation was performed using the fitness landscape exactly as in (ZELDOVICH et al. 2007) where replication rate is a constant as long as all proteins are at least marginally stable. In this case, the lethal mutagenesis threshold is a constant value of around 2.5, essentially independent on the number of rate determining genes (Figure 3C). This finding is consistent with
(Zeldovich et al. 2007) which also predicted that lethal mutagenesis threshold (counted as number of mutations per genome per generation) is independent on the genome size for the flat fitness landscape at $\Delta G < 0$. The reason for slight numeric discrepancy of 20% between the analytical prediction and simulations is due to the effect of coupling of mutations and replications. Furthermore, as can be observed in figure 3C, with the elimination of slow replication regime (in the control simulation all viable organisms are always replicating with the same speed), the lethal mutagenesis threshold is significantly reduced as well. This is exactly because slowly replicating organisms make extinction less likely in a given finite amount of time.

Therefore, our results, as indicated in Figures 3B and C suggest that even under optimal growth conditions for bacteria, when the natural death rate is negligible, there still exists a certain lethal mutagenesis threshold for the species. Moreover, our results shown in Figure 3B indicate that the lethal mutagenesis threshold increases and plateaus when the number of rate determining genes increases.

For semi-conservatively replicating viruses we also consider a variable death rate which can range from 10% of the initial average population birth rate to 90% of the initial average population birth rate. As we can see in Figure 4A, in the presence of this finite death rate, the lethal mutagenesis threshold is significantly reduced. As natural death rate increases from 10% to 90% of the replication rate, the lethal mutagenesis threshold for a population of organisms with 20 rate determining genes decreases from 2.8 mutations per replication to around 0.5 mutations per replication. (see Figure 4A).

**Lethal Mutagenesis for Conservative Replication (for RNA Viruses)**
Some RNA viruses may replicate conservatively. In our numerical simulation, we use a simplified model for conservative replication whereby one master genome is preserved while the descendent genome might undergo certain mutations. Our results showed that in this case viruses can sustain higher mutation rates before reaching lethal mutagenesis threshold compared to semi-conservatively replicating organisms.

RNA viruses usually have small genomes; many of them contain around a dozen or so of proteins, we therefore consider most of RNA virus genes as rate determining (Sanjuan et al. 2004). Here we take their number as twenty and study the lethal mutagenesis threshold for conservatively replicating viruses as a function of viral natural death rate. As shown in Figure 4B, the threshold decreases quickly with the increase of natural death rate.

Our numerical simulation actually showed that under the same natural death rate and same numbers of rate determining genes, the conservative replication’s lethal mutagenesis threshold would be around 15% greater than twice lethal mutagenesis threshold for the semi-conservatively replicating organisms. Therefore the coupled mutation-replication scenario affects conservative replication by shifting lethal mutagenesis threshold slightly upwards compared to the analytical prediction for the uncoupled case.

**Distribution of protein stabilities in evolved populations.**

After evolving in a steady thermal environment for a sufficient time, the distribution of protein stabilities within an organism reaches equilibrium, as shown in Figure 5A.
An important new finding from our calculations is that the mutation rate significantly affects the stationary stability distributions for all proteins in a population. When mutation rate is increased, more and more proteins become marginally stable. Moreover, as we can see from Figure 5A, at low mutation rate, which is the case for most DNA based organisms, protein stability distribution in our simulation agrees very well with the stability distribution of real proteins drawn from the experimental database, which is a considerable improvement compared with previous analytical model (ZELDOVICH et al. 2007).

**DISCUSSION**

In this work, we systematically studied lethal mutagenesis for several biological systems and discussed the effect of various parameters, such as mutation rate, death rate, number of rate determining genes, and replication mechanisms, on the lethal mutagenesis threshold.

Our model is based on a minimal biologically reasonable assumption that the organismal replication rate is determined by the concentration of functional (i.e. correctly folded) rate determining proteins, and that loss of stability by any of these would result in a lethal phenotype. When all rate determining proteins in the organism are stable and properly folded, the organismal replication rate is high, and the population growth is fast. However, deleterious or beneficial mutations may occur during the replication process. A deleterious mutation in our model is one that increases the folding free energy of a rate determining protein, destabilizing it and decreasing the number of its properly folded copies in the organism, leading to a decreases of the replication rate. Furthermore, a
deleterious mutation could also result in a protein having folding free energy greater than zero, which is lethal to the organism. In this case, the organism would not be able to survive and would eventually die.

Our results showed that the lethal mutagenesis threshold increases and plateaus with the number of rate determining genes. On the other hand, the threshold could be made smaller with an increase in the natural death rate for the organism. Therefore, our work might potentially lead to more directed search for bacterial lethal mutagenesis (Bull and Wilke 2008). Although previous lethal mutagenesis experiments have been more focused on RNA viruses, recently several experiments have also been carried out on bacterial systems with increased mutation rates (Sniegowski 1997). However, these bacteria usually exhibit unchanged fitness or some beneficial mutation traits, rather than decreased fitness, in the stable environment of the experimental set-up. The advantageous effect of higher mutation rates which are still well below the lethal mutagenesis threshold was also found in recent ab initio microscopic simulations of model cells (Heo et al. 2009). This is because, although the elevations in the mutation rate in these systems are between 10-fold and 100-fold over their wild-type mutation rates (Drake et al. 1998; Sniegowski et al. 1997), they are still well below the lethal mutagenesis threshold and therefore could lead to fixation of beneficial mutations by hitchhiking instead of extinction.

However, lethal mutagenesis is still potentially achievable in bacteria. In our model, we observed that the lethal mutagenesis threshold could be reduced by choosing a bacterium species with fewer number of rate determining genes, in an environment with a non-negligible natural death rate. For example, for a bacterium or DNA virus species
with 20 rate determining genes and a death rate equal to 20% of the initial replication rate, the lethal mutagenesis threshold is roughly 2.1 mutations per genome per replication. Even though this number is still above the current level of the observable bacterial mutation rate, exploring bacteria’s lethal mutagenesis in various experimental settings can still lead to basic insights about mutation, replication rate, and organismal fitness; therefore may be well worth the effort.

We also separately considered lethal mutagenesis in DNA-based organisms and RNA-based organisms. Our results showed that given the same natural death rate, organisms with conservative replication mechanisms, such as RNA viruses, could tolerate a higher mutation load than DNA-based organisms with a semi-conservative replication mechanism, in accord with the prediction of the analytical theory (ZELDOVICH et al. 2007). Experimentally, ribavirin is the drug commonly considered a candidate for causing lethal mutagenesis in RNA viruses (CROTTY et al. 2002; FREISTADT et al. 2004). Many experiments have focused on introducing ribavirin to retroviruses such as HIV, hepatitis C, the vesicular stomatitis virus (VSV), etc. This often leads to an increased mutation rate and possibly, the lethal mutagenesis of such viruses. As shown by Crotty et al. in 2001 (CROTTY et al. 2001), a population of polioviruses can become 90% extinct at exactly six mutations per genome per replication, while the normal mutation rate for this virus is approximately one mutation per genome per replication. This is in agreement with our prediction of around 6.2 mutations per genome per replication for RNA viruses with 15 proteins controlling the replication rate and a natural death rate equal to 25% of the wild type’s replication rate.
In recent years, many studies of lethal mutagenesis were based on the original model of Muller’s ratchet (Gessler 1995; Haigh 1978; Rouzine et al. 2008). Although these models provided many useful insights on various aspects of adaptation and mutation, our model is different in that we link the fundamental genotypic property – protein stability - with the phenotype and do not employ the selection coefficient and other a’priori unknown parameters. Here we infer fitness directly from the stabilities of rate determining proteins of the organism and relate the death phenotype to the loss of structure (and therefore function) of key proteins.

Recently Bull et al. proposed a model of lethal mutagenesis of bacteria and viruses (Bull et al. 2007; Bull and Wilke 2008). In their model, the extinction threshold for bacteria is 0.69 deleterious mutations per genome per replication, and the threshold for viruses is different from ours too. A possible reason for such difference is that they only considered deleterious mutations, whereas we considered all mutations affecting protein stability, which may be beneficial deleterious or neutral. In our model, a beneficial mutation makes a rate determining protein more stable, providing more copies of properly functioning proteins in the cell. Beneficial mutations constitute a significant fraction among all point mutations in our model, therefore it is very important to take them into consideration. The beneficially mutated strains will then have a higher replication rate and be farther from the ‘‘death boundary’’ and therefore produce more offspring. Meanwhile, we also allow mutations occurring in different proteins to interfere with each other through their cumulative effect on fitness Eq.2, and the dynamics of multiple mutations are taken into account. However, it is worthwhile to compare our prediction of around 3 mutations per organism per duplication for semi-conservative
mechanism with that of Bull et al.’s prediction of 0.69 deleterious mutations per organism per duplication. Notice that in the fitness landscape model employed here, the probability to have a deleterious mutation (the one that has $\Delta \Delta G > 0$) among all possible mutations is roughly 71%. Given this condition, 3 mutations per organism per replication roughly correspond to 2 deleterious mutations per organism per replication. Moreover, considering the effect of back mutations and the ability for beneficial mutations to increase fitness in our model, the effective “rate-decreasing” mutation number should be even smaller than 2 here. We thus note that our result is slightly different than that of Bull et al, but the two numbers are of the same order of magnitude.

The major conceptual difference between our model and several models rooted in formal population genetics including Muller ratchet and recent study of Bull and coauthors (BULL et al. 2007; BULL and WILKE 2008) is that in our model the main cause of lethal mutagenesis is in actual mutation-induced death events: Cells or viruses can literally die when they acquire lethal mutations which make one of their proteins unstable. In contrast in other models the lethal mutagenesis occurs when replication rate falls below a certain threshold. For that reason one should not expect the results from the two approaches to exactly match each other.

The effect of protein stability on phenotype was considered in our earlier analytical theory (ZELDOVICH et al. 2007). To make the model tractable we did not consider the coupled mutation-replication process there. Although this approximation works well at low mutation rates, it becomes less quantitatively accurate at high mutation rates. While the analytical theory in (ZELDOVICH et al. 2007) provided a qualitatively correct estimate for the lethal mutagenesis threshold, our present study shows that these
estimates may be 15-20% off more accurate numbers based on simulations of coupled replication-mutation events and in a more realistic fitness landscape given by Eq.2. Thus a coupled mutation-replication model is essential for more accurate estimate of lethal mutagenesis threshold, which occurs at high mutation rates per replication where the analytical approximation of (ZELDOVICH et al. 2007) remains qualitatively but not quantitatively correct.

Many earlier experimental works (ANDERSON et al. 2004; CROTTY et al. 2001) associated the lethal mutagenesis in RNA viruses with ‘‘error catastrophe’’ predicted by Eigen and coworkers for the quasispecies model (EIGEN et al. 1989). According to this model at high mutation rates the population loses fitness by delocalizing in sequence space (EIGEN et al. 1989). However, it was argued in (ZELDOVICH et al. 2007) and demonstrated in (HEO et al. 2009) that error catastrophe in the quasispecies model is a consequence of a highly unrealistic single fitness peak assumption. On the other hand close agreement between lethal mutagenesis threshold predicted here and in and the observed one (CROTTY et al. 2002) makes it highly plausible that the physical cause of lethal mutagenesis is the persistent loss of stability of one or more of essential proteins at higher mutation rates.

Another important result of our model is prediction of distribution of stabilities of proteins in evolved populations, without adjustable parameters and in almost perfect agreement with experiment (see Figure 5A). Analytical theory predicted the distribution of stabilities which was in good but not perfect agreement with reality. In particular the peak of the predicted distribution was shifted towards lower stabilities compared to experiment, and analytical distribution overall predicted a greater number of marginally
stable proteins than observed in experiment. There could be three possible reasons for the discrepancy between analytical results and experiment: 1) bias in the ProTherm database reflecting overall difficulties of experimental study of marginally stable proteins 2) That the assumption of the analytical theory that evolutionary processes had reached steady state may not be fully justified and 3) That the ‘‘step- function like’’ fitness landscape used in the analytical theory is too oversimplified by not taking into account the gradual loss of fitness as proteins become marginally stable. The present study indicates that 3) is the right reason for the discrepancy between analytical prediction and experiment. When we took into account that low stability proteins essentially lead to lower fitness due to lower fraction of folded (and therefore functional) essential proteins, the agreement between predicted and observed distribution of stabilities very much improved without introducing additional adjustable parameters. Apparently lower fitness at higher proportion of marginally stable proteins gives rise to additional pressure leading to the shift of the distribution towards somewhat more stable proteins.

Our study, as well as previous analytical work provide a realistic explanation to the observation that most proteins are not exceedingly stable – indeed the distribution of protein stabilities peaks around -5kcal/mol (see Figure.5A). Several authors attributed such moderate stability to the functional requirement of flexibility which calls for lower stability of a protein. An observation that stabilities of natural proteins are not too high was suggested as an evidence for the coupling between function and stability (DEPRISTO et al. 2005). However the problem with this argument is that it is based on the assumption that any observed behavior of proteins has adaptive causes. As noted in our earlier work (ZELDOVICH et al. 2007) as well as by others (BLOOM and ARNOLD 2009; BLOOM et al.
the observed range stabilities of natural proteins can be explained without assuming a selective advantage of any particular value of stability.

Experiments show that increasing stability by site-directed mutagenesis does not affect biological function of a protein. A number of earlier works which seemed to suggest otherwise have been sometimes seriously misinterpreted. In most cases of these earlier studies (see e.g. (Beadle and Shoichet 2002; Shoichet et al. 1995)) only active site residues were mutated and indeed loss of activity accompanied by some stabilization of the protein was observed for several mutations. However this result suggests only that carving active site (often enriched with polar and/or charged amino acids) on a surface of an enzyme may indeed destabilize the protein. However in order to prove that limited stability of a protein is a prerequisite of its function one has to study the functional effect of stabilizing mutations outside the active site and show that these also lead to loss of function. These experiments are necessary to separate the indirect effect of mutations on function through stability alteration from a direct effect on function due to mutations in the active site. When a protein was mutated outside the active site the increase of stability did not result in a loss of activity (Bloom et al. 2006). Our study provides another evidence for independence of stability and activity of proteins, by accurately predicting the distribution of proteins stabilities without assuming any relation between the two.

Taverna and Goldstein (Taverna and Goldstein 2002) argued that protein stability is not too high for entropic (in sequence space) reason: That there are much more sequences corresponding to proteins of low to moderate stability than to more stable ones. A similar observation was made by Bloom et al in their study of neutral evolution of
protein stability (BLOOM et al. 2007). While this argument is certainly a correct one, it does not explain why the distribution of proteins stabilities has a well-defined peak around -5kcal/m rather than being shifted towards less stable proteins whose sequences represent an overwhelming majority. Our study answers this question by showing that distribution of protein stabilities is established as a compromise between two opposing factors: A) physical factors which favor less stable proteins for entropic (in sequence space) reasons outlined in (TAVERNA and GOLDSTEIN 2002) and B) population genetics pressure which favors more stable proteins by eliminating from populations organisms which carry marginally stable proteins. The organisms whose genotypes encode more marginally stable proteins become eliminated from populations for two reasons: 1) their fitness is lower because the fraction of folded proteins is diminished and, more importantly, 2) because organisms with less stable proteins are closer to “death” boundary i.e. they leave less viable progeny.

A new insight coming from this study is the dependence of stability of proteins in a population of organisms on mutation rates. Our simulations predict that species with higher mutation rates (such as RNA viruses) should have less stable proteins than their lower mutations rates counterparts. The underlying reason for this finding is that mutations which destabilize proteins are deleterious in our model. At low mutation rates purifying selection dominates and organisms carrying destabilizing mutations are purged from the population – hence the distribution of protein stabilities is shifted towards more stable proteins. As mutation rates get higher the supply of deleterious mutations increases and purifying selection is no longer capable to purge all mutants from the population – hence the distribution shifts towards less stable proteins. The observed dependence of
protein stability on mutation rate $m$ arises only in the regime $Nm \gg 1$, otherwise purifying selection is able to purge any destabilizing mutant from the population. Further, we note that this effect is due to continuous dependence of fitness on proteins stability (i.e. inhomogeneous generation time) as given by Eqs (1,2). In our earlier study with step-function fitness landscape where mutations are neutral as long as $\Delta G < 0$, the long-time distribution of protein stability was independent on mutation rates (ZEDOVICH et al. 2007). Our results can also be contrasted with earlier studies of mutational robustness which predicted that higher mutation rates would lead to emergence of more robust proteins (BORNBERG-BAUER and CHAN 1999; VAN NIMWEGEN et al. 1999). In these studies strictly neutral mutations were considered while in our model strictly neutral mutations do not exist as there is a direct relation between protein stability and fitness.

A recent study by Tawfik and coauthors provides some support to our prediction – showing that the attributes of proteins stability such as contact density - are significantly different in proteins of RNA viruses than that of DNA-based organisms (TOKURIKI et al. 2009). However, as suggestive as it is, the work of Tawfik et al (TOKURIKI et al. 2009) is not a proof of lower stability of RNA viral proteins: A much more comprehensive analysis based on throughput measurements of proteins stabilities in several organisms is required to confirm or falsify this prediction.

Finally, we note that our model of lethal mutagenesis is minimalist in that it did not account for various important biological processes, such as gene recombination, Darwinian selection due to competition for limited resources, or interaction between an organism and external factors. For example, ribavirin has been demonstrated to have at least three activities in vivo or in cell culture, including inhibition of cell replication,
immunomodulatory effects, and incorporation as a mutagenic nucleoside by the viral RNA polymerase (Crotty et al. 2002). Therefore, further efforts and extensions, such as more explicit consideration of protein function, protein-protein interactions, or the structure-function relationship, would also be valuable to the understanding of lethal mutagenesis in bacteria and viruses.

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Table 1. Assumptions about species replication in our model.

|                   | Duplication Mechanism                                                                 | Death Rate       | Rate determining gene number |
|-------------------|--------------------------------------------------------------------------------------|------------------|------------------------------|
| Bacteria          | Semi-Conservative, mutations could happen to both descendent copies                   | Negligible       | Large (20~300)               |
| DNA Virus         | Semi-Conservative (mostly), mutations could happen to both descendent copies          | Non-negligible   | Small (~20)                  |
| RNA Virus         | Conservative (mostly), mutations only happen to one descendent copy, a master genome is preserved | Non-negligible   | Small (~20)                  |

Table 2. Similarities and differences between this model and traditional population genetics models

|                                           | Our Model                                           | Traditional Models                                           |
|-------------------------------------------|-----------------------------------------------------|--------------------------------------------------------------|
| Beneficial versus Deleterious Mutation   | beneficial mutations and back mutations allowed     | Mutations are deleterious, back mutations not allowed        |
| Relationship between Mutation and Fitness | Mutations decrease fitness on average, but beneficial and back mutations also exist. | Mutations decrease fitness, wild-types are the fittest      |
| Dependence on Genome Size                 | Larger genomes lead to more rate-determining proteins, potentially increase robustness | Independent of genome size                                  |
| Selection Criteria                        | All essential proteins must fold properly           | Absent of deleterious mutations, or fewer than k mutations per organism |
| Generation Time                           | Taken into consideration                            | Considered in some models, but not always considered         |
**FIGURE CAPTIONS**

**Figure 1.** Scatter plot of $\Delta \Delta G$ versus the wild-type $\Delta G$ values taken from the ProTherm database. 2188 data points of independent point mutation experiments were plotted. The dependence of $\Delta \Delta G$ on $\Delta G$ is weak ($R=0.11$). The apparent narrowing of the distribution at low stabilities is due to the fact that mutations leading to $\Delta G > 0$ cannot be expressed.
Figure 2. Population dynamics with different mutation rates for a bacterium with 20 rate-determining proteins (Dotted line, 4 Mutations/Duplication; Solid Line, 3 Mutations/Duplication).
Figure 3. The effect of the number of rate determining genes. A. Population dynamics with different rate-determining genes, with the mutation rate fixed at 3 mutations per
organism per duplication. (Blue line: 10 proteins; green line, 50 proteins; red line, 100 proteins). When the number of rate-determining genes is low, the population becomes extinct very quickly, whereas when it is high, the population can have sustainable growth.

**B. Lethal mutagenesis threshold** $m_c$ as a function of $\Gamma$ for semi-conservative replication.

As the number of rate-determining genes increases, the mutagenesis threshold grows as well. The threshold shows tendency of saturation with increased number of rate-determining proteins.

**C. Mutagenesis threshold** $m_c$ as a function of the number of genes, in the control simulation whereby the duplication rate is set to constant independent on protein stabilities. Here the lethal mutagenesis threshold is roughly constant, and about 20% lower than the analytical prediction because of the coupled mutation-duplication effect in this simulation.
Figure 4. A. Lethal mutagenesis threshold $m_c$ as function of $D_n$ - natural death rate for DNA viruses. This simulation is performed for organisms with 20 rate-determining genes. The natural death rate is measured as a ratio probability of death of a progenitor at each duplication event to the birth rate. B. Lethal mutagenesis threshold as a function of natural death rate for RNA viruses, with number of rate-determining genes set at 20.
Figure 5. A. Distribution of protein stabilities in bacterial species with high and low mutation rates. (Bars: Experimental Data compiled from the ProTherm database (Kumar et al. 2006); Blue Line: Low mutation rate case, 0.1 Mut/Genome/Replication; Green Line: Analytical model prediction from (Zeldovich et al. 2007); Red line: High mutation rate case, 2.5 Mut/Genome/Replication). The number of rate determining genes is fixed at 20. B. Stability of all proteins averaged over all organisms in a population versus mutation rate in mutations per genome per replication.
