Water hammer and column separation induced by simultaneous and delayed closure of two valves

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Water hammer and column separation induced by simultaneous and sequential (delayed) closure of two valves may occur in industrial pipeline systems. This paper deals with such cases both experimentally and numerically. Water hammer equations are solved by the method of characteristics. Transient cavitating pipe flow is simulated by a discrete gas cavity model (DGCM) that considers unsteady skin friction. Discrete gas cavities and Zielke's convolution-based unsteady skin friction term are explicitly incorporated in the staggered grid algorithm of the method of characteristics. Experiments have been performed in a laboratory pipeline apparatus. The apparatus consists of an upstream end tank, a horizontal steel pipeline (total length 55.37 m, inner diameter 18 mm), four valve units positioned along the pipeline including the end points, and a downstream end tank. A transient event is induced either by simultaneous or sequential closure of two end valves. Numerical results are compared and verified with results of measurements. In addition, a theoretical analysis of pressure wave fronts travelling along the pipeline is also presented to clearly show profound effects of wave interactions.

Keywords: pipeline, two valves, simultaneous and delayed valve closure, water hammer, column separation, experimental setup, unsteady friction

Highlights

• Water hammer and column separation events induced by simultaneous and sequential (delayed) closure of two valves were investigated.
• Experimental test rig is presented and described in detail.
• Discrete gas cavity model is validated against experimental results.
• Pressure wave fronts travelling along the pipeline for cases with and without friction and transient cavitation were analyzed theoretically.

0 INTRODUCTION

The term hydraulic transients means a process that takes place in a physical system during the transition from one to another steady state. Knowledge of hydraulic transients and conditions that cause extreme pressures are crucial for safe and economical design of hydraulic systems. Hydraulic transients occur during opening and closing of control valves and changing of the operating mode of hydraulic turbomachinery such as turbo pumps and water turbines [1] and [2]. As a result of these changes high or low pressures are formed and transferred through the hydraulic pipe system with a speed which is close to the speed of sound in liquids. The local speed of sound is defined by the physical condition of the liquid (free air content) and pipe wall (rigid, elastic) and usually is variable in time and space. Pressure waves may have such intensity that they can lead to serious malfunctions of hydraulic system equipment and can cause significant damages and even breakdown of system components. To prevent unwanted effects of hydraulic transient events, pipeline systems must be fitted with adequate protective surge control means. The term water hammer is a synonym for rapid unsteady flow in pipelines and was named after the characteristic sound that occurs during the unsteady event and sounds like strikes with a hammer.

For understanding water hammer phenomena, except pressure changes, fluid compressibility and pipeline mechanics must be considered [1] and [2]. The side effects of water hammer are transient cavitation and column separation, unsteady skin friction, fluid-structure interaction (FSI) and viscoelastic behaviour of the pipe wall [3]. During transient events, it may happen that liquid pressure drops to the liquid vapour pressure. In this case vapour bubbles form [4]. Liquid also contains a certain amount of free and dissolved gas, and if the value of pressure in the system drops below the gas saturated pressure it leads to gas releasing from the liquid and the occurrence of gaseous cavitation [5]. Thus, formed vapour and gas bubbles can coalesce, form large pockets and cause separation of the liquid flow in the pipeline (column separation). The positive pressure waves reflected from the system boundaries (e.g., reservoir, valve,
turbine, pump, etc.), compress the bubbles in the cavitation-flow region and progressively reduce the size of the cavity produced by column separation [4]. Cavities collapse and the re-joining of separated columns may produce very high pressures higher than the pressure initially given by the Joukowsky equation and may cause damage of the system components [1]. The value of the friction factor, which describes the resistance due to pipe-wall friction during transients, is different from its value for the steady state flow. For fast transients, the friction coefficient \( f \) can be expressed as the sum of two parts: the quasi-steady part \( f_q \) and the unsteady part \( f_u \) [8] to [10]. The unsteady part attempts to represent velocity profile changes and flow regime conversions from laminar to turbulent and vice versa [9] to [10].

The objective of this paper is to investigate and discuss water hammer and column separation effects induced by simultaneous and sequential (delayed) closure of two end valves in a simple pipeline apparatus. There are many industrial pipeline systems with multiple-valves, at least with two of them. Multiple actions of valves may induce very large or low pressure waves due to superposition of the waves [11]; therefore, engineers try to avoid it. However, there are reports on the usage of single or even multiple-check valves to attenuate column separation effects [12] and [13]. Recent investigations show that closure of two end valves may produce less severe column separation induced pressure fluctuations than the classical case with the downstream end single valve closure only [14]. In addition, different positions of the valves [15] and their controlled action (water hammer interferometer) [16] may attenuate pressure oscillations significantly.

The paper starts with mathematical tools for water hammer, transient cavitation and unsteady friction including boundary conditions and continues with the description of the experimental setup. In the second part of the paper, water hammer and column separation results from two valve closure experimental runs are compared with computed results. The paper concludes with a theoretical analysis of pressure wave fronts travelling along the pipeline for two end valve closure cases that include the effects of skin friction and transient cavitation.

1 THEORETICAL MODELLING

A simplified version of the continuity and momentum equations, neglecting the convective terms, is used to describe unsteady pipe liquid flow [1]:

\[
\frac{\partial Q}{\partial t} + gA \frac{\partial H}{\partial x} + RQ|Q| = 0,
\]

\[
a \frac{\partial Q}{\partial t} + gA \frac{\partial H}{\partial x} = 0,
\]

where unknown variables are piezometric head \( H \) and discharge \( Q \); friction coefficient is defined as \( R=f/(2DA)\).

Solving Eqs. (1) and (2) numerically with the method of characteristics (MOC) gives the following compatibility equations:

\[
\frac{dQ}{dt} + \frac{gA}{\alpha} \frac{dH}{dt} + RQ|Q| = 0,
\]

\[
\frac{dQ}{dt} - \frac{gA}{\alpha} \frac{dH}{dt} + RQ|Q| = 0.
\]

Eqs. (3) and (4) are valid along the characteristic lines \( dx/dt = \pm \alpha \) (Fig. 1).

![Fig. 1. Characteristic lines in x-t plane](image)

It is assumed that the head, \( H \), and discharge, \( Q \) at time \( t \) are known. These may be either initially known (i.e., at \( t_0=0 \), initial conditions), or they were calculated during the previous time step. It is necessary to compute the unknown values of \( H \) and \( Q \) at time \( t+\Delta t \). Referring to Fig. 1, for known values of \( Q \) and \( H \) at points A and B it is necessary to determine their values at point P. Numerically solving Eqs. (3) and (4) along the lines AP and BP leads to [1]:

\[
H_P = C_P - B_P(Q_{d,P}),
\]

\[
H_P = C_M - B_M(Q_{d,P}),
\]

where:

\[
C_P = H_A - B(P_Q)A,
\]

\[
B_P = B(R(Q_{d,P})),
\]

\[
C_M = H_C - B(Q_{d,B}),
\]

\[
B_M = B + R(Q_{d,B}).
\]

where \( B = \alpha/gA \) is the pipeline characteristic impedance which depends upon the pipe properties.
Eq. (5) is referred as the *positive characteristic equation* and Eq. (6) as the *negative characteristic equation* [1].

1.1 Boundary Conditions

Boundary conditions describe relationships that define the discharge or head at a boundary, or a relationship between the head and discharge at the boundary. At the downstream end of the small-scale pipeline apparatus (Fig. 2), \( x=L \), combining equations for the discharge through the ball valve V3/3H, \( Q_p = C_{bh} \sqrt{A H_{bh}} \) and the needle valve V3/3C, \( Q_p = C_{nc} \sqrt{A H_{nc}} \), and the positive characteristic equation, Eq. (5) gives:

\[
Q_p = \frac{2 C_C}{C_b + \sqrt{C_b^2 + 4 C_C}} \quad \text{if} \quad C_b > 0, \tag{11}
\]

\[
Q_p = \frac{1}{2} \left(-C_b + \sqrt{C_b^2 + 4 C_C} \right) \quad \text{if} \quad C_b < 0, \tag{12}
\]

where:

\[
C_b = \frac{C_{m}^2 C_{bh} B_p}{C_{m}^2 + C_{bh}^2}, \quad C_c = \frac{C_{m}^2 C_{bh} C_p}{C_{m}^2 + C_{bh}^2}. \tag{13}
\]

The boundary condition at the upstream end, \( x=0 \), is defined by combining expressions for the discharge through the ball valve V0/3U (Fig. 2) and the negative characteristic equation, Eq. (6). Taking into account a constant pressure head in the high-pressurized tank, a quadratic equation is obtained, which roots are Eqs. (11) and (12) with:

\[
C_b = C_{bh} B_M, \quad C_c = C_{bh} (C_M - H_{rev}). \tag{14}
\]

1.2 Discrete Gas Cavity Model

Up to date, several mathematical and numerical models for modeling of vaporous and gaseous cavitation in pipelines have been developed. The discrete gas cavity model (DGCM) [2] is used in this paper. The DGCM can successfully simulate vaporous cavitation if the amount of a free gas in the liquid is small (gas void fraction \( \alpha_g \leq 10^{-7} \)) [2], [4]. The model allows gas and vapour cavities to form at all computational sections in the MOC grid. A liquid phase with a constant wave speed \( a \) is assumed to occupy the reaches connecting the computational sections. A discrete gas cavity is described by two water hammer compatibility equations (Eqs. (5) and (6)), the continuity equation for the cavity volume:

\[
\frac{d \varphi_g}{dt} = Q_{out} - Q_n, \tag{15}
\]

and the ideal gas equation with the assumption of isothermal behaviour of the free gas [2]:

\[
\varphi_g = \alpha_g \varphi \left( \frac{P_0}{P_g} \right). \tag{16}
\]

A detailed description of the DGCM and its numerical solution is given in [2]. The MOC based DGCM algorithm in this paper incorporates an improved computationally effective Zielke’s convolution-based (with quasi-2-D weighting function) unsteady friction model [17]. Zielke’s weighting function for transient laminar flow [18] and Vardy-Brown weighting functions for transient turbulent flow [19] to [21] are used in the numerical simulations.

2 EXPERIMENTAL SETUP

Experimental research was conducted in a small-scale pipeline apparatus for investigation of water hammer events including column separation and fluid-structure interaction [22].

The apparatus is comprised of a horizontal pipeline that connects the upstream end high-pressurized tank to the outflow tank (steel pipe of total length \( L = 55.37 \text{ m} \); internal diameter \( D = 18 \text{ mm} \); pipe wall thickness \( e = 2 \text{ mm} \); maximum allowable pressure in the pipeline \( p_{\max, \text{at}} = 25 \text{ MPa} \)) – see Fig. 2. Four valve units are positioned along the pipeline including the end points. The valve units at the upstream end tank (position 0/3) and at the two equidistant positions along the pipeline (positions 1/3 and 2/3) consist of two hand-operated ball valves (valves Vi/3U and Vi/3D; \( i = 0,1,2 \)) that are connected to the intermediate pressure transducer block. The air pressure in the upstream end tank can be adjusted up to 800 kPa. The pressure in the tank is kept constant during each experimental run by using a high-precision fast-acting air pressure regulator (precision class: 0.2 %) in the compressed air supply line. Four dynamic high-frequency pressure transducers are positioned within the valve units along the pipeline including the end points (see Fig. 2). Pressures \( p_{0/3}, p_{1/3}, p_{2/3} \) and \( p_{3/3} \) are measured by Dytran 2300V4 high-frequency piezoelectric absolute pressure transducers (pressure range: from 0 MPa to 6.9 MPa; resonant frequency: 500 kHz; acceleration compensated; discharge time constant: 10 seconds (fixed)). The datum level for all pressures measured in the pipeline and at the tank is at the top of the
horizontal steel pipe (elevation 0 m in Fig. 2). The water temperature is continuously monitored by the thermometer installed in the outflow tank. The water hammer wave speed was determined as \( a = 1340 \text{ m/s} \pm 10 \text{ m/s} \) [26]. The fast closing electro-pneumatically operated ball valve (V3/3P) is controlled with filtered compressed air which is supplied through a plastic pipeline from the pressure regulator, in which the pressure is independent from the rest of the system. The transient event can be triggered by fast closing or opening of the downstream end valve, using either the V3/3P or the V3/3H. Both valves are equipped with a fast-response displacement sensor (measurement range: 0° to 90°, frequency response: >10 kHz) which measures the change of the valve angle (\( \alpha \)) during its closing or opening. In addition, transients can be induced by closing or opening hand-operated valves along the pipeline (valves V\(i\)/3U and V\(i\)/3D; \( i = 0, 1, 2 \)). At the upstream end high-pressurized tank and at the downstream end of the pipeline, two strain-gauge pressure transducers (\( P_{0/3-sg} \) and \( P_{3/3-sg} \); pressure range: from 0 MPa to 1 MPa, uncertainty: ±0.5 %) are installed. These transducers are used for the evaluation of the initial conditions in the system. The needle valve (V3/3C) is used for adjustment of the initial pipe discharge. The initial discharge (velocities larger than 0.3 m/s) is measured by the electromagnetic flow meter (uncertainty: ±0.2 %). All measured data are collected by the data acquisition system (sample rate: up to 100 kHz) that is connected to a PC. In the cases presented in the paper, transients were induced by ‘simultaneous’ closure of 1) the hand-operated ball valve at the downstream end of the pipeline and 2) the hand-operated ball valve at the upstream end (V3/3H+V0/3U). The pressure in the upstream tank was 400 kPa and initial pipe velocities were 0.3 m/s and 2.12 m/s. This apparatus has been classified as an unsteady friction dominated apparatus [22] because the Ghidaoui’s parameter [23] is close to 1. The relative importance of unsteady friction for the two case studies is indicated by the Duan’s parameter [24]: \( I = 0.007 \) for \( V_0 = 0.30 \text{ m/s} \) and \( I = 0.05 \) for \( V_0 = 2.12 \text{ m/s} \). The effects of unsteady friction for rapid transients are important when \( I < 0.1 \).

![Fig. 2. Layout of small-scale pipeline apparatus](image-url)
3 EXPERIMENTAL AND NUMERICAL RESULTS

A number of experiments have been performed in the laboratory pipe system (Fig. 2) for better understanding of unsteady flow phenomena caused by the closure of two valves. The valve closures were induced ‘simultaneously’ as much as possible by using valve V3/3H at the downstream end of the pipeline and valve V0/3U at the upstream end. Results from two distinct experimental runs are presented and compared with calculated results in this section: 1) water hammer case and 2) column separation case. Transients were induced first by a fast closure of the downstream end valve V3/3H and second by a delayed fast closure of the upstream end valve V0/3U. The sampling frequency for each continuously measured quantity was $f_s = 3,000 \text{ Hz}$.

3.1 Water Hammer Case

Fig. 3 presents measured and computed pressure head traces in the laboratory pipeline apparatus ($H_{3/3}, H_{2/3}, H_{1/3}$ and $H_{0/3}$) for the rapid closure of the two valves for the initial flow velocity $V_0 = 0.3 \text{ m/s}$; the effective valve closure times were much less than the wave reflection time $2L/a = 0.08 \text{ s}$. This experimental run represents the water hammer case (pressure head is above the vapour pressure head at all times).

The fast closure of the downstream end valve (V3/3H) produces the classical Joukowsky pressure head rise $\Delta H_{\text{max}} = 41.3 \text{ m}$. The second delayed fast closure of the upstream end valve (V0/3U) produces a pressure head rise at this valve of practically the same magnitude. The time delay between the two valve closures is 0.036 s and the time difference between the two measured maximum heads is 0.03 s (due to different valve closure times of 40 ms and 34 ms, respectively). The maximum head due to the closure of V0/3U occurs within the second water hammer time period ($L/a < t < 2L/a$). The maximum measured head $H_{\text{max}} = 83.0 \text{ m}$ occurs at the downstream end valve as a short duration pressure pulse superimposed on the third bulk pressure pulse and it is slightly larger than first bulk head of 80.0 m. Overall, there is good agreement between measured and computed results.

3.2 Column Separation Case

Fig. 4 shows measured and computed head traces in the pipeline apparatus ($H_{3/3}, H_{2/3}, H_{1/3}$ and $H_{0/3}$) for the fast closure of the two valves for the initial flow velocity $V_0 = 2.12 \text{ m/s}$. In this case column separation
occurs in the system. Again the valve closure times were less than the wave reflection time $2L/a = 0.08$ seconds (V3/3H: 70 ms and V0/3U: 65 ms).

The column separation case produces water hammer with column separation including large cavities and extended regions of distributed vaporeous cavitation along the pipeline. The initial fast closure of the downstream end valve (V3/3H) produces the classical Joukowksy pressure head rise $\Delta H_{\text{max}} = 277.9$ m. The second delayed fast closure of the upstream end valve (V0/3U) produces a pressure head drop from the reservoir head to the vapour pressure head of $-9.8$ m. The time delay between the two end valve closures is 0.34 s. At the time of the pressure drop at V0/3U the water flows from the reservoir towards the downstream end. The pressure heads along the pipeline remain practically constant at the vapour pressure head for a longer period. The first fast closure of the downstream end valve (V3/3H) produces the maximum pressure head $H_{\text{max}} = H_0 + \Delta H_{\text{max}} = 310.3$ m in the system. The results obtained using the DGCM give pressure histories that are in good agreement with the experimental results. Reopening of one or both valves at selected time(s) after the closing periods is subject of the authors’ future work.

Fig. 5 shows the responses of the reservoir-pipeline-valve and reservoir-valve-pipeline-valve system of Fig. 2 considering two theoretical cases: 1) the first one is an ideal frictionless system without cavitation and 2) the second one is system without cavitation but with consideration of unsteady skin friction (water hammer case). The steady flow is stopped 1) by instantaneous downstream end valve closure and 2) by instantaneous simultaneous or sequential (delayed) two end valve closures. The initial flow conditions are the same as for the water hammer case in Section 3.1 with the initial flow velocity $V_0 = 0.30$ m/s. Figs. 5a and b show the case of V3/3H valve closure (V0/3U stays open). The unsteady friction obviously produces attenuation of pressure waves and also rounds pressure pulses. Comparison of quasi-steady and unsteady friction effects has been previously shown in [11]. Timing of the pressure waves is practically unaffected by friction effects. The pressure at the position $x/L = 0$ has a constant value equal to the reservoir pressure. Effects of unsteady friction show similar behavior for the case of the simultaneous closure of the two valves.
Fig. 5. Comparison of theoretical dimensionless heads (without and with friction) at the end valves \((x/L = 1 \text{ and } 0)\) and at the midpoint \((x/L = 0.5)\); \(V_0 = 0.3 \text{ m/s; } p_{eq} = 400 \text{ kPa}\)
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5 THEORETICAL ANALYSIS OF PRESSURE WAVES  
IN FRICTIONLESS PIPE AND FRICTION DOMINATED PIPE  
INCLUDING EFFECTS OF CAVITATION  
(COLUMN SEPARATION CASE)

Far more complex is the case with transient cavitating pipe flow (column separation). Comparison of theoretical dimensionless heads without and with consideration of unsteady friction is shown in Fig. 6.  
As for the water hammer case, (Section 4), the steady flow is stopped 1) by instantaneous downstream end valve closure and 2) by instantaneous simultaneous or sequential (delayed) closure of two end valves. The initial flow conditions are the same as for the column separation case in Section 3.2 with the initial flow velocity \( V_0 = 2.12 \text{ m/s} \).

The effects of cavitation and unsteady friction for the case of V3/3H closure (V0/3U stays open) are depicted in Figs. 6a and b. It is obvious that cavitation limits the minimum pressure head to the liquid vapour pressure head at the position \( x/L = 1 \) where cavitation starts at 2L/a. The pressure head at \( x/L = 0 \) stays at the reservoir pressure head at all times. The pressure head at \( x/L = 0.5 \), after cavitation starts at the time 2.5L/a, fluctuates between the initial and the vapour pressure head with a period of L/a. No doubts that cavitation has a predominant effect on the pressure response. For the case of the simultaneous closure of the two valves (Figs. 6c and d) the effects of cavitation play a major role again. Unsteady friction contributes to slight attenuation and timing of bulk pressure pulses. Naturally the minimum pressure heads along the pipeline are limited to the liquid vapour pressure head. As described previously in Section 4, instantaneous V0/3U closure at time L/a after V3/3H closure results in a constant high pressure along the pipeline. Therefore, cavitation does not appear in this case and this is clearly depicted in Figs. 6e and f. System response for the case of 1.5 L/a delayed V0/3U closure after V3/3H is closed is even more profound (Figs. 6g and h). The pressure response at \( x/L = 1 \) and \( x/L = 0 \) is similar with a delay of L/a to each other. At \( x/L = 0.5 \) (midpoint of the pipeline) cavitation occurs at time 3L/a and lasts for 0.5L/a. After that no cavitation exists at the midpoint. The second valve closure with a time delay of 4L/a produces longer periods of cavitation existence along the pipeline (Figs. 6i and j). At \( x/L = 1 \) cavitation starts at time 2L/a and lasts until 7.5L/a. At \( x/L = 0 \) cavitation also occurs at 2L/a after V0/3U is closed and exists for a longer period. Similar behaviour can be observed at the midpoint of the pipeline too. Finally, the two valve closure case with cavitation exhibits its profound effect on pressure.
Fig. 6. Comparison of theoretical dimensionless heads (without and with friction) at the end valves (x/L = 1 and 0) and at the midpoint (x/L = 0.5); V₀ = 2.12 m/s; pₑ = 400 kPa

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response while unsteady friction only slightly affects the amplitude, shape and timing of the pressure pulses.

7 CONCLUSIONS

Water hammer and column separation effects triggered by simultaneous and sequential (delayed) closure of two end valves have been investigated in a laboratory pipeline apparatus. A numerical discrete gas cavity model (DGCM) with inclusion of the convolution-based unsteady friction term has been successfully validated against the investigated experimental runs including water hammer and column separation cases. Finally, a novel theoretical analysis of pressure wave fronts travelling along the pipeline triggered by simultaneous and delayed closure of the two end valves for cases without and with friction and transient cavitation has been presented. It has been shown that unsteady friction affects rounding and attenuation of pressure head pulses but has no major impact on their timing. Effects of cavitation on pressure histories are far more profound because they include liquid rupture, waves and shocks. Depending on the second valve closure delay cavitation may be a long or short lasting event. In some cases (V0/3U, L/a delayed closure) cavitation does not occur at all.

In the near future, the authors are planning to improve the experimental setup by installing one additional fast closing electro-pneumatically operated ball valve instead of V0/3U and a new PLC (programmable logic controller). In this way simultaneous and controlled sequential closure of the two electro-pneumatically operated ball valves will be possible thus enabling further experimental, numerical and theoretical investigations in the relatively new field of controlled multiple valve actions in pipelines.

8 NOMENCLATURES

| Symbol | Definition |
|--------|------------|
| A      | cross-sectional area, [m²] |
| a      | wave speed, [m/s] |
| B      | pipeline characteristic impedance, [m²s] |
| BM     | constant of positive characteristic equation, [m³/s] |
| BP     | constant of negative characteristic equation, [m³/s] |
| C      | discharge coefficient, [-] |
| CM     | constant of positive characteristic equation, [m] |
| CP     | constant of negative characteristic equation, [m] |
| D      | pipe internal diameter, [m] |
| E      | Young’s modulus of elasticity, [N/m²] |
| e      | pipe wall thickness, [m] |
| f      | friction coefficient, [-] |
| g      | gravitational acceleration, [m/s²] |
| H      | piezometric head (head) |
| I      | Duan’s parameter, [-] |
| L      | length, [m] |
| N      | number of computational reaches, [-] |
| p      | pressure, [N/m²] |
| Q      | discharge, [m³/s] |
| R      | friction coefficient, pipe bend radius, [1/m³], [m] |
| V      | flow velocity, [m/s] |
| x      | axial distance, [m] |
| α      | valve opening angle, [°] |
| a_g    | volume fraction of gas in mixture with a fluid, [-] |
| ΔH     | losses at the valve, pressure head increase, [m] |
| ∀      | volume, [m³] |

Subscripts:
0  initial conditions
d  downstream
bv  ball valve
g  gas
in  inlet
max  maximum value
nv  needle valve
out  outlet
q  quasi-steady
res  reservoir
u  unsteady, upstream

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