Unveiling the optical properties of a metamaterial synthesized by electron-beam-induced deposition

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Abstract
Direct writing using a focused electron beam allows for fabricating truly three-dimensional structures of sub-wavelength dimensions in the visible spectral regime. The resulting sophisticated geometries are perfectly suited for studying light–matter interaction at the nanoscale. Their overall optical response will strongly depend not only on geometry but also on the optical properties of the deposited material. In the case of the typically used metal–organic precursors, the deposits show a substructure of metallic nanocrystals embedded in a carbonaceous matrix. Since gold-containing precursor media are especially interesting for optical applications, we experimentally determine the effective permittivity of such an effective material. Our experiment is based on spectroscopic measurements of planar deposits. The retrieved permittivity shows a systematic dependence on the gold particle density and cannot be sufficiently described using the common Maxwell–Garnett approach for effective medium.

Keywords: electron beam induced deposition, metamaterials, nanocomposite

(Some figures may appear in colour only in the online journal)
focused electron beam is capable of delivering three-dimen-
sional features, smaller than tens of nanometer in a highly
flexible and precise single-step process [8–10]. The electron
beam induced deposition (EBID) process is based on local
decomposition of inserted precursor-gas molecules by an
electron beam within a vacuum chamber of a scanning elec-
tron microscope. Since typical precursors are of the metal-
organic type, not only their metallic constituents remain after
deposition, although this would be the ideal case. Instead, a
substantial amount of ligand components as well as elements
of the residual gas in the vacuum chamber (carbon, oxygen
and hydrogen) are incorporated [8, 11]. Thus, the resulting
composite can be viewed as a metamaterial or an effective
material by itself, consisting of single-crystalline nano-
particles (e.g. gold) embedded in a carbonaceous matrix [10].
While the electric properties of granular materials such as the
EBID material are well understood [12] and proved to be
promising for sensing applications [13, 14], a complete
optical description of EBID metamaterials based on a com-
bined experimental and theoretical study has not been
reported yet. This is caused by the relatively small areas
which can be conventionally fabricated with the EBID pro-
cess, not allowing for optical characterization with standard
methods such as ellipsometry. First attempts using micro-
ellipsometry showed a behaviour close to a Maxwell–Garnett
effective medium for a gold-containing EBID material [15].
Recently, the Maxwell–Garnett theory was also used to
describe material properties of helices made of platinum-
EBID composite [16] to numerically study their circular
dichroism. While the overall agreement between experiment
and numerical simulations was reasonable, distinct deviations
became obvious for both the long wavelength range and the
actual strength of the observed optical activity [16]. This trend
was also emphasized in a numerical study of similar com-
posite materials [17].

Here, we present the results of spectrometric measure-
ments in combination with a numerical algorithm based on
the transfer-matrix approach for retrieval of the permittivity
of gold-EBID $10 \times 10 \mu m^2$ pad-like deposits (see figure 1(c)).
The investigation concerns deposits of different thicknesses to
systematically study the dependence of the permittivity on the
density of the nano-inclusions in the carbonaceous matrix. In
addition, the comparison of analytical results based on Mie
theory with an effective medium model such as Maxwell-
Garnett proves that although the dipole resonance of the gold
particles dominantly contributes to the optical response of
the EBID composite, the conventional Maxwell-Garnett approach
cannot be employed to describe the effective optical proper-
ties of the composite. The presented experimentally retrieved
permittivity is expected to give better understanding of optical
performance of nanostructures fabricated via EBID, paving
the way for sophisticated nano-optic applications.

2. Sample preparation

The experimental investigation started with the fabrication of
a substrate which consists of a $170 \mu m$ thick glass (BK7) plate

![Figure 1](image_url). (a) Microscopy setup for spectral measurements of EBID nanopads. The sample is illuminated with white light emitted by a halogen-lamp. A beam splitter (BS) between the lamp and the first microscope objective (MO) guides part of the reflected light onto a detector. The central part of the nanopad is imaged onto a pinhole with a diameter of 600 $\mu m$ placed in front of the detectors. (b) Cross-
section through the nanopad and the substrate (layer thicknesses are not drawn to scale). (c) Scanning electron micrograph of an investigated EBID pad.

with a conductive thin layer of indium tin oxide (ITO) on top.
Both materials were characterized using ellipsometry and show typical properties. The same ellipsometry measurement was used to determine most accurately the thickness of the ITO coating (36 nm).

The EBID process itself was carried out in a vacuum
chamber of a dual-beam instrument (FEI Strata DB 235)
equipped with a gas-injection system for dimethyl-gold(III)acetyl-acetonate ($Me_2Au(acac)$) as the precursor gas [18]. The injected precursor molecules adsorb, diffuse and desorb onto the sample surface where they are locally cracked by the focused electron beam [19]. Thereby, the EBID technique not
only allows for the realization of complex three-dimensional geometries [16, 20] but also for depositing them on even non-
planar substrates, if these are at least weakly conductive [10].
During the molecule dissociation, their non-volatile parts
form the deposit while the volatile constituents are pumped
out [18].

The deposition process depends on the energy and cur-
rent of the electron-beam, and on the dwell time (the time the
beam resides at each position) as well as on the scanning
raster. All these factors were previously optimized for fabri-
cation of high-resolution three-dimensional nanostructures
[10]. The aim in the current work was to keep the deposition
parameters of the pad deposits as close as possible near the
range used for nanostructures to unveil their material prop-
erties. Correspondingly, the retrieved permittivity reliably
describes the material of nanostructures written by EBID.

5 Commercial ITO-on-glass substrate was avoided due to undefined thickness of the ITO coating and its pronounced crystallinity causing strong scattering effects.

6 see supporting information available at stacks.iop.org/nano/27/025705/mmedia.
Since the optimized parameters would lead to an unrealistically long deposition time for such deposits, the dwell time was drastically reduced down to 1 μs and the lateral sizes were restricted to $10 \times 10 \, \mu m^2$ while maintaining the other parameters (see scanning electron micrograph of a typical EBID pad in figure 1(c)). For the systematic investigation, EBID deposits with thicknesses ranging from 15 nm up to 50 nm (far below the Fabry–Pérot cavity condition) were fabricated and topographically characterized by atomic force microscopy (AFM). The AFM scans confirmed that at the edges all pads have increased thickness with respect to the perfectly smooth and flat interior. This is caused by the low pressure of the precursor gas [18], resulting in a mass-transport-limited (also called molecule-limited) deposition regime [21–23]. In this regime all available precursor molecules within the square deposition region are consumed and dissociated by the primary and the secondary electrons. This leads to a decreased deposition rate in the central area as well as to stronger co-deposition of carbon from the residual chamber gases [19, 24]. The diffusion of the intact precursor molecules outside the irradiated region causes an increased precursor supply at the edges, leading to enhanced deposition there [22]. Hence, each fabricated pad exhibits a $9 \times 9 \, \mu m^2$ large surface area of high quality and constant thickness. These were utilized for spectroscopic measurements in an optical microscopic setup.

3. Methods

To measure optical spectra, a home-built microscopic setup was used (see figure 1(a)). A halogen lamp emitted unpolarized and noncoherent light within the spectral range of interest between 480 nm and 900 nm. The sample was illuminated using a $60 \times$ microscope objective, which also collected the reflected light. For separation of the incident and the reflected light, a beam splitter was used between the source and the objective. The position of the microscope objective relative to the sample surface was carefully adjusted to obtain plane-wave illumination at normal incidence and to image the sample surface onto the detector plane. The area of interest could be selected using a pinhole in the image plane. The size of this additional aperture was chosen to be 600 μm in diameter, guaranteeing the measurement of the signal solely from the flat inner part of the deposit, while maintaining a sufficient signal-to-noise ratio. Each EBID pad was measured separately by placing it on the optical axis such that the propagation of the incoming plane-wave was normal with regard to the sample surface. In the same way, the light transmitted through the sample was measured.

The experimental scheme described above permits interpreting the measurement data as spectra of reflected ($I_R$) and transmitted ($I_T$) intensities of an incoming plane-wave ($I_0$) by a multilayer system (see figure 1(b)). Such a structure can be analytically described using a transfer matrix (see footnote 6): 

$$
\begin{bmatrix}
I_R \\
I_T
\end{bmatrix} = 
\begin{bmatrix}
R_{EBID}R_{ITO}R_{glass} & T_{EBID}T_{ITO}T_{glass} \\
T_{EBID}T_{ITO}T_{glass} & R_{EBID}R_{ITO}R_{glass}
\end{bmatrix}
\begin{bmatrix}
I_0 \end{bmatrix}.
$$

(1)

where $R$ and $T$ are reflection and transmission matrices describing propagation and multiple reflection of light within the EBID layer, the ITO layer and the glass substrate, respectively. Each matrix contains information about the geometrical (thickness $d$) and optical (permittivity $\varepsilon$) properties of the corresponding layer. The only unknowns in the equation above are the real and imaginary part of $\varepsilon_{EBID}$. All further parameters describing the ITO-on-glass substrate as well as the EBID layer thicknesses are determined experimentally. Consequently, the optical properties of the EBID material can be retrieved from measurements of reflection and transmission. Due to the sub-wavelength thickness, the light within the EBID and the ITO layers ($R_{EBID}$, $R_{ITO}$, $T_{EBID}$ and $T_{ITO}$) must be described as coherent [25] in the investigated spectral range. In contrast, the glass substrate is two orders of magnitude thicker than $\lambda$. Therefore, and due to the used light source, light propagation across the entire sample requires a semi-coherent description [26]. Furthermore, according to equation (1) the measured values $I_R$ and $I_T$ have to be normalized with respect to the incident intensity $I_0$. To this end, the reflection from and the transmission through the ITO-on-glass substrate was measured and the theoretical reflectance and transmittance coefficients were calculated (see footnote 6).

Though the calculation of the sample’s reflectance and transmittance is straightforward if the complex permittivity of the EBID layer is known, the inverse problem is not. In addition, there are several distinct variations of $\varepsilon_{EBID}$ which result in the same reflectance and transmittance of the sample. Therefore, this inverse problem was tackled using a brute force search, i.e., calculating the reflectance and transmittance of the sample for several thousand possible complex values of $\varepsilon_{EBID}$ for each wavelength and comparing them with the experimental results. Thereby, all local minima in the two-dimensional permittivity-space corresponding to the respective smallest deviation from the measured spectra were identified. By subsequent refining of the region around the minima, several steady solutions of $\varepsilon_{EBID}(\lambda)$ were found. However, there is only one physical solution which has to be determined. Accordingly, all dispersions which exhibit a constant increase of the real part of the refractive index ($dRe[n]/d\lambda = const$ where $n = \sqrt{\varepsilon}$) in the whole investigated spectral range are excluded. Such solutions have unrealistically high values and appear repeatedly while extending the plane of possible solutions (see footnote 6). In contrast, the only dispersion which does not follow this tendency has values in a reasonable range and meaningfully reflects the inner structure of the EBID composite.
4. Results and discussion

Figure 2(a) shows the experimental reflectance and transmittance data of the EBID–ITO–glass system for different deposit thicknesses. All reflectance spectra exhibit distributions with a maximum value observed at around 620 nm, which slightly red-shifts for increasing layer thickness. Likewise, the transmittance spectra feature minima at around 550 nm and also show the expected decrease in transmittance for thicker pads. The corresponding real and imaginary parts of the retrieved permittivity are presented in figure 2(b) for the sake of clarity, the measurement noise is removed by fitting the retrieved real and imaginary parts of \( \varepsilon_{\text{EBID}}(\lambda) \) with a polynomial function. The green curve of the thinnest deposit is expected to approximate the best material properties of nanostructures, fabricated with EBID.

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This observation is consistent with a chemisorption of the gold-containing precursor molecules onto the sample surface together with possibly decreasing vapour pressure over the long deposition times [19, 24]. As mentioned, the concave shape of the pads implies a mass-transport-limited deposition regime [22] in which excess electrons start to dissociate residual gases—mainly hydrocarbons present in the vacuum chamber. For typical vacuum pressures around \( 10^{-6} \) hPa, still a large number of molecules sufficient to form one monolayer per second impinge onto the substrate only from the residual gases [19] and possibly due to a longer resident time of some precursor-gas ligands at the irradiated spot [21]. Thereby, after the depletion of the chemisorbed initial layer, the codeposition of carbon, oxygen and hydrogen becomes dominant and increases the relative carbon content in the thicker pads. For a long deposition time, this effect becomes particularly important if the precursor vapour pressure decreases with time. Thus, the carbon content of the deposits
rises along with the deposition time and with the deposit thickness [24]. As a consequence, properties of the EBID composite can be tuned by the density of the gold inclusions, from strongly dielectric to slightly metallic optical behaviour.

In that respect, the permittivity of the thinnest pad is expected to correspond to the material properties of nanostructures which can be fabricated using EBID. Fine structures (e.g. pillars or needles) are fabricated optimally with a dwell time even up to 720 μs, initiating local heating, while staying in the mass-transport-limited deposition regime. Furthermore, the slender geometry, together with the overall short deposition time, supports the heating effect, which ensures a relatively high content of gold around 28 at% [10].

Concerning the spectral characteristic of the retrieved permittivity, the prominent resonance in Im[ε_EBID] at around 650 nm can be attributed to the dipole resonance of the gold nanoparticles within the carbonaceous matrix. The mean particle diameter of the singly crystalline particles varies around 4 nm ranging approximately from 2 nm to 7–8 nm with a decreasing number of larger particles [10, 27]. Correspondingly, figure 3 shows Mie cross-sections of absorption (blue line) and of scattering (brown line) for isolated spherical gold particles of a mean diameter of 4 nm with a lognormal size distribution of 50% standard deviation under plane-wave illumination (see footnote 6). The EBID matrix is approximated by non-absorbing diamond [28] (solid line) while gold properties are taken from [29]. As expected, the Mie cross-sections are dominated by an absorptive dipole resonance around 630 nm, which corresponds to the absorption properties retrieved for the EBID matrix. In this size regime the shift of the resonance position due to the nanoparticle size distribution is negligible. Thus, the Mie resonance is comparatively narrow, indicating that the broadening of the metamaterial resonance is due to further loss mechanisms besides the effect of the size distribution and the intrinsic absorption of the gold inclusions. In that respect, absorption of the carbonaceous matrix as well as interaction between the particles, which are not included in the classical Mie approach, play a significant role. Careful analytical considerations [30] show that tiny losses of the matrix will not only slightly red-shift the peak position but also cause strong broadening of the resonance. Therefore, losses of the carbonaceous matrix, especially for the thicker deposits, are responsible for the very broad resonance of Im[ε_EBID].

Based on these results, description of ε_EBID(λ) using an effective medium approach based on dipoles in a dielectric environment seems to be promising. Considering the inner structure of the EBID material (randomly distributed metallic nanocrystals of deep sub-wavelength dimensions within a dielectric matrix), the Maxwell–Garnett theory [31] constitutes the obvious choice. For that purpose the matrix material is described as amorphous carbon [32] to account for the matrix loss, and gold properties are taken again from [29]. Since the actual value of the volume filling factor of gold in the composite is not known, it can therefore act as tuning factor. Figure 4 shows the comparison between the retrieved permittivity of the thinnest pad and the Maxwell–Garnett effective media for three different values of filling factor: 15%, 20%, 25%. None of the possible combinations can reproduce the retrieved ε_EBID(λ). Neither tuning of the filling factor nor substitution of the material properties of gold and the carbonaceous matrix (including absorption) from other material databases significantly changes the output of the Maxwell–Garnett calculations. This indicates that the EBID composite does not meet the Maxwell–Garnett conditions [17, 31]. Indeed, the particles can be safely described within the quasistatic approximation; the absorptive dipole-type resonance fits well to the Maxwell–Garnett approach considering pure dipole–dipole interaction under the assumption of negligible scattering. However, well separation of the particles, required by the Maxwell–Garnett cannot be taken for granted. The close spacing between the gold inclusions

![Figure 3](image3.png)

**Figure 3.** Mie scattering and absorption cross-sections of isolated gold particles embedded in diamond environment under plane-wave excitation. The particles have a mean diameter of 4 nm with a lognormal size distribution of 50% standard deviation.

![Figure 4](image4.png)

**Figure 4.** Comparison of the retrieved permittivity of the EBID material (green) with the Maxwell–Garnett effective medium theory for three different volume filling fractions of 15%, 20% and 25%.
will presumably cause both, not only near-field interactions [17], but also local electron tunnelling through the carbonaceous matrix. As proven for the electrical applications of EBID materials, the gold nanocrystals are not electrically isolated within the carbonaceous matrix, but instead, electron transport, due to thermally assisted tunnelling of electrons, takes place [13]. Furthermore, the mass-limited deposition regime and hence the varying amount of co-deposited carbon influences the local particle density. An appropriate choice for the extension of Maxwell–Garnett seems to be the introduction of self-consistency, and thereby the iterative correction of the properties of the carbonaceous matrix by the effective permittivity itself [33]. In addition, the formation effect of differently shaped particle aggregates and their influence of higher order multipolar contributions need to be accounted for as well [17, 34]. However, considering all these effects together and due to the lack of knowledge concerning the optical properties of the carbonaceous matrix, a consistent effective material approach relying on only few and physically meaningful parameters still represents a significant challenge.

5. Conclusions

In summary, the dielectric function of an EBID material consisting of single-crystalline gold particles dispersed in a carbonaceous matrix is studied experimentally. The retrieved effective permittivities show a systematic dependence on the layer thickness and, thus, the particle density within the deposit. The effective permittivity for the highest metal content represents the best approximation of the material properties of EBID nanostructures. While the prominent absorption feature present in the retrieved imaginary parts of the EBID permittivities could be attributed to the dipole resonances of the embedded gold nanoparticles via Mie calculations, the optical properties of the material cannot be described by using a standard Maxwell–Garnett approach. Remarkably, this material also shows a very interesting optical behaviour at wavelengths around 450 nm where the real part of its permittivity exhibits a zero-crossing, which might require more attention. While the presented study is based on Me₃Au(acac) as an exemplary gas precursor, the discussed method can be applied to any type of EBID-based metamaterial fabricated using metal-organic precursors. Thereby, the numerical and experimental study of complex nanostructures made of EBID metamaterials can be envisaged.

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