Observations of Laboratory and Natural Slow Slip Events: Hikurangi Subduction Zone, New Zealand

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Abstract Slow slip events (SSEs) are recognized as an important component of plate boundary fault slip, and there is a need for laboratory friction data on natural samples to guide comparisons with natural SSEs. Here, we compile a comprehensive catalog of SSEs observed geodetically at the Hikurangi subduction zone offshore northern New Zealand, and compare it with results of laboratory friction experiments that produce laboratory SSEs under plate tectonic driving rates (5 cm/yr). We use samples from Ocean Drilling Program Site 1124 seaward of the Hikurangi subduction zone to represent the plate boundary that hosts shallow SSEs at Hikurangi. We find that laboratory SSEs exhibit a similar displacement record and range of stress drops as the natural SSEs. Results of velocity step tests, which can be used to evaluate frictional instability based on the critical stiffness criterion, indicate that the slow slip activity at Hikurangi is a form of stably-accelerating slip. Our laboratory SSEs provide an alternative method of quantifying (in)stability by direct measurement of the unloading stiffness during the stress drop. The observed dependence of laboratory SSE parameters on effective normal stress is consistent with critical stiffness theory; however, depth-increasing projections based on laboratory data do not match observations from natural SSEs. These differences are likely related to changing temperature and fault rock composition downdip but also complications related to scaling and/or limited sampling. Scientific drilling recently undertaken at the Hikurangi subduction zone should serve to improve and guide future studies of the role of frictional properties for the occurrence of SSEs.

1. Introduction

Although slow fault slip events have been observed for decades (e.g., Goulty & Gilman, 1978; Ihmlé & Jordan, 1994; Linde et al., 1988; Sacks et al., 1978, 1981), improved and widespread geodetic observations have rapidly increased understanding of these phenomena over the past ~20 years. Slow and transient fault slip occurs over a wide range of timescales, from long-term slow slip events (SSEs) with durations on the order of years, to low-frequency earthquakes that are fast enough to be detected seismologically (Ide et al., 2007; Peng & Gomberg, 2010). SSEs are considered important due to their impact on the seismic cycle; however, the exact nature of the relationship between slow slip and seismic slip is unclear. In some cases, SSEs are thought to increase earthquake hazard by loading adjacent fault patches (Kaneko et al., 2018; Koulaei et al., 2017; Mazzotti & Adams, 2004; Reynolds & Bannister, 2007; Wech & Creager, 2011). Earthquakes can also trigger SSEs (Wallace et al., 2017, 2018) even if the triggering earthquake is small (Han et al., 2014); conversely, they can also arrest SSEs (Wallace et al., 2014). The location of SSEs in some subduction zones suggests that they delineate locked zones, perhaps revealing the region of future coseismic ruptures (Chapman & Melbourne, 2009; Dixon et al., 2014; Wallace & Beavan, 2010). In other cases, they can occur on the seismogenic portion of the subduction megathrust (Ito et al., 2013; Larson et al., 2007; Ruiz et al., 2014). One particular region with well-documented SSEs is the Hikurangi subduction zone offshore New Zealand, which is the focus of this study.

The variability of SSEs and their complex relationship with ordinary earthquakes has prompted discussion on the mechanisms and conditions for SSE occurrence (e.g., Saffer & Wallace, 2015). Laboratory measurements of fault frictional properties are an essential component of studies targeting fault slip behavior. Measuring how the frictional strength of a fault depends on the slip velocity provides an indication as to...
whether a fault will slide stably or unstably, with unstable faults expected to produce ordinary earthquakes (e.g., Dieterich, 1986; Dieterich & Kilgore, 1996; Marone, 1998; Scholz, 2002). Based on this framework, SSEs are proposed to be related to the transition between unstable and stable frictional regimes (e.g., Lowry, 2006; McCaffrey et al., 2008; Rubin, 2008). A recent experimental development is the ability to shear samples at geologically realistic driving rates of cm/yr, simulating the natural driving rate boundary condition of plate-boundary faults (Ikari, Ito, et al., 2015; Ikari & Kopf, 2017). These experiments have revealed that at tectonic plate rates, spontaneous perturbations in stress and slip rate occur that resemble geodetic observations of natural SSEs. This facilitates comparison between natural and laboratory SSEs, and measurements of frictional properties may provide insight into the mechanism behind SSEs. Here, we present the results of laboratory friction experiments utilizing driving velocities as low as 5 cm/yr, conducted on a sample of sediment recovered from the subducting plate ~400 km east of the Hikurangi subduction margin. The lithologic unit is typical of the incoming sediment section and is likely representative of the shallow decollement at the northern Hikurangi subduction margin, where seafloor geodetic studies have documented SSEs to within at least 2 km of the seafloor (Wallace et al., 2016). We compare characteristics of natural SSEs in the Hikurangi region with observations from laboratory SSEs, with the goal of constraining the mechanism of natural SSEs, and providing a first step toward linking laboratory and observational data sets.

2. Hikurangi Subduction Zone, New Zealand

The Hikurangi subduction zone is located off the east coast of New Zealand’s North Island (Figure 1). It is formed by westward subduction of the Pacific plate at a rate of 2–6 cm/yr (Wallace et al., 2004). This margin has hosted megathrust earthquakes with moment magnitude $M_w$ of up to 7.1, but none larger over the past century (Doser & Webb, 2003). However, indications of geodetic locking (Figure 1b) suggest that the plate interface could rupture in earthquakes of $M_w$ 8 or larger (Wallace et al., 2009).

Notably, this region is one of the best studied examples of a subduction zone that hosts frequent SSEs, which have been detected geodetically since 2002 by a continuous Global Positioning System (cGPS) network (Bartlow et al., 2014; Douglas et al., 2005; McCaffrey et al., 2008; Wallace et al., 2009, 2012, 2014, 2016, 2018, 2017; Wallace & Beavan, 2006, 2010; Wallace & Eberhart-Phillips, 2013). A striking characteristic of the Hikurangi SSEs is the clear separation at ~40–41°S between shallow SSEs (<15 km depth) in the northern Hikurangi Trench, and deeper SSEs (~30–60 km depth) to the south (Figure 1b; Tables 1 and 2). In general, the shallower events are shorter (2–3 weeks) and more frequent (every 1–2 years), while deep events are
| Event and Year          | Duration (Days) | Depth of Maximum Slip (km) | Maximum Slip D (mm) | Stress Drop (kPa) | Drop Peak Slip Velocity V (cm/yr) | Event V/Vo | Downdip Width (km) | D/r | Mw | Reference       |
|------------------------|-----------------|----------------------------|---------------------|-------------------|----------------------------------|------------|--------------------|-----|----|------------------|
| Gisborne Nov 2004      | 17              | 12.0                       | 180                 | 51.7              | 386.5                            | 193.2      | 46                 | 7.8E-06 | 6.3 | Wallace & Beavan, 2010 |
| Tolaga Bay Dec 2004    | 20              | 3.5                        | 40                  | 1.4               | 73.0                             | 36.5       | 93                 | 8.6E-07 | 6.0 | Wallace & Beavan, 2010 |
| S. Hawkes Bay June 2006| 7               | 12.0                       | 40                  | 1.9               | 208.6                            | 104.3      | 72                 | 1.1E-06 | 6.1 | Wallace & Beavan, 2010 |
| Gisborne July 2006     | 6               | 12.0                       | 40                  | 2.8               | 243.3                            | 121.7      | 87                 | 9.2E-07 | 6.3 | Wallace & Beavan, 2010 |
| S. Hawkes Bay August 2006 | 7       | 9.6                        | 220                 | 19.2              | 1147.1                           | 573.6      | 81                 | 5.4E-06 | 6.6 | Wallace & Beavan, 2010 |
| N. of Gisborne Dec 2007| 34              | 10.0                       | 90                  | 6.2               | 96.6                             | 48.3       | 62                 | 2.9E-06 | 6.2 | Wallace & Beavan, 2010 |
| S. Hawkes Bay March 2008| 5            | 12.0                       | 30                  | 1.6               | 219.0                            | 109.5      | 52                 | 1.1E-06 | 6.1 | Wallace & Beavan, 2010 |
| Mahia Mar 2008         | 15              | 12.8                       | 85                  | 4.5               | 206.8                            | 103.4      | 78                 | 2.2E-06 | 6.4 | Wallace & Beavan, 2010 |
| Tolaga Bay Aug 2008    | 12              | 9.0                        | 45                  | 3.3               | 136.9                            | 68.4       | 61                 | 1.5E-06 | 6.1 | Wallace & Beavan, 2010 |
| Tolaga Bay + Mahia Feb 2010 | 14      | 9.0                        | 120                 | 7.4               | 312.9                            | 156.4      | 84                 | 2.9E-06 | 6.4 | Wallace & Beavan, 2010 |
| Gisborne March 2010    | 16              | 13.0                       | 125                 | 8.8               | 285.2                            | 142.6      | 70                 | 3.6E-06 | 6.4 | Wallace & Beavan, 2010 |
| Cape Tumagain 2011     | 32              | 9.6                        | 100                 | 5.1               | 114.1                            | 57.0       | 105                | 1.9E-06 | 6.5 | Wallace et al., 2012 |
| Hawkes Bay 2011        | 20              | 15.0                       | 40                  | 3.3               | 73.0                             | 36.5       | 65                 | 1.2E-06 | 6.1 | Wallace et al., 2012 |
| Tolaga Bay 2011        | 21              | 12.0                       | 60                  | 6.7               | 104.3                            | 52.1       | 36                 | 3.3E-06 | 5.9 | Wallace et al., 2012 |
| Gisborne 2011          | 11              | 12.0                       | 55                  | 4.3               | 182.5                            | 91.3       | 66                 | 1.7E-06 | 6.2 | Wallace et al., 2012 |
| Hawkes Bay/Cape Turnagin 2013 | 12       | 9.0                        | 240                 | 15.1              | 730.0                            | 365.0      | 91                 | 5.3E-06 | 6.5 | Wallace & Eberhart-Phillips, 2013 |
| Tolaga Bay 2013        | 20              | 9.0                        | 150                 | 15.2              | 273.8                            | 136.9      | 52                 | 5.8E-06 | 6.2 | L. Wallace unpublished data |
| Gisborne 2014          | 24              | 7.0                        | 270                 | 21.7              | 410.6                            | 205.3      | 33                 | 1.6E-05 | 6.5 | Wallace et al., 2016 |
| East Coast triggered SSE 2016 | 14     | 7.5                        | 130                 | 1.5               | 338.9                            | 169.5      | 92                 | 2.8E-06 | 6.8 | Wallace et al., 2017 |

Stress drop and M_w calculated assuming a shear modulus of 10 GPa. V_o = 2.0 cm/yr, r = half the downdip width. V_o = initial slip velocity (cm/yr), r = downdip half width (km), M_w = moment magnitude.
| Event Year (Stage) | Duration (Days) | Depth of Maximum Slip (km) | Maximum Slip D (mm) | Stress Drop (kPa) | Peak Slip Velocity (cm/yr) | Event V/Vo | Downdip Width (km) | D/r | Mw | Reference |
|-------------------|-----------------|-----------------------------|---------------------|------------------|--------------------------|------------|-------------------|-----|----|-----------|
| Kapiti 2003       | 202             | 53                          | 200                 | 111.3            | 36.1                     | 24.1       | 48                |     |    | Wallace & Beavan, 2010 |
| Manawatu (stage 1)| 2004            | 53                          | 230                 | 55.8             | 23.0                     | 15.3       | 97                |     | 6.9 | Wallace & Beavan, 2010 |
| Manawatu (stage 2)| 2004            | 50                          | 200                 | 39.6             | 121.7                    | 81.1       | 104               |     | 6.9 | Wallace & Beavan, 2010 |
| Manawatu (stage 3)| 2004            | 50                          | 190                 | 43.5             | 57.8                     | 38.5       | 89                |     | 6.8 | Wallace & Beavan, 2010 |
| **Manawatu total**| **2004**        | **545**                     |                     |                  |                          |            |                   | 7.2 |    |           |
| Kapiti 2008 (stage 1)| 2004        | 53                          | 80                  | 26.4             | 24.3                     | 16.2       | 48                |     | 6.3 | Wallace & Beavan, 2010 |
| Kapiti 2008 (stage 2)| 2004        | 53                          | 270                 | 128.7            | 164.3                    | 109.5      | 69                |     | 6.7 | Wallace & Beavan, 2010 |
| Kapiti 2008 (stage 3)| 2004        | 38                          | 110                 | 32.1             | 44.6                     | 29.7       | 73                |     | 6.6 | Wallace & Beavan, 2010 |
| Kapiti 2008 (stage 4)| 2004        | 38                          | 60                  | 24.6             | 12.2                     | 8.1        | 60                |     | 6.4 | Wallace & Beavan, 2010 |
| **Kapiti 2008 total**| **2004**      | **450**                     |                     |                  |                          |            |                   | 7.0 |    |           |
| Manawatu 2010/11 (stage 1)| 2004      | 53                          | 55                  | 11.1             | 22.3                     | 14.9       | 81                |     | 6.5 | Wallace et al., 2012   |
| Manawatu 2010/11 (stage 2)| 2004      | 38                          | 160                 | 31.8             | 48.7                     | 32.4       | 95                |     | 6.9 | Wallace et al., 2012   |
| Manawatu 2010/11 (stage 3)| 2004      | 38                          | 90                  | 23.1             | 13.7                     | 9.1        | 83                |     | 6.7 | Wallace et al., 2012   |
| **Manawatu 2010/11 total**| **2004**    | **450**                     |                     |                  |                          |            |                   | 7.1 |    |           |
| Kapiti 2016 (still ongoing)| 2004      | 300                         | 220                 | 53.7             | 26.8                     | 17.8       | 88                | 5.0E-06 | 6.9 | Wallace et al., 2018   |

Stress drop and M\textsubscript{w} calculated assuming a shear modulus of 30 GPa. V\textsubscript{o} = 1.5 cm/yr, r = half the downdip width. V\textsubscript{o} = initial slip velocity (cm/yr), r = downdip half width (km), M\textsubscript{w} = moment magnitude.
longer (>1 year), and less frequent (recurrence of ~5 years) (Wallace et al., 2009, 2012; Wallace & Beavan, 2010). The difference in depths of occurrence for shallow and deep SSEs coincides with the depth of geodetic plate locking along the margin. The shallow SSEs largely occur at the mostly creeping (e.g., decadal scale creep, or averaged over multiple SSE cycles) northern and central Hikurangi margin, while the deep SSEs wrap around the large, locked seismogenic zone at southern Hikurangi (Figure 1b).

Geophysical logging, coring, and observatory installations were recently undertaken along a transect of drill sites spanning the Hikurangi plate boundary in late 2017 and early 2018 during IODP Expeditions 372 and 375 (Wallace et al., 2019). Prior to these expeditions, scientific drilling in this region was limited to the sedimentary sequence on the subducting Pacific plate (~400 km east of the Hikurangi Trough) that was drilled during ODP Leg 181, at Site 1124 (Carter et al., 1999). Although the goals of Expedition 181 did not focus on plate-boundary fault behavior, the incoming sediments at subduction zones are expected to be similar to those which constitute the shallow megathrust fault and are thus a valuable resource for investigating the mechanical behavior of the shallow plate boundary (e.g., Hüpers et al., 2017; Ikari et al., 2018; Underwood, 2007). The sample we use is a mixture of three core samples (20X-5, 21X-5, and 22X-5) from Site 1124, which span a recovery depth from ~195 to 215 meters below seafloor (mbsf); this is the same sample used in a recent friction study by Rabinowitz et al. (2018). Lithologically, all three samples are described as a clay-bearing nanofossil chalk with mudstone interbeds, which is generally representative of the majority of the sediment column recovered at Site 1124 (Carter et al., 1999). Following the method described in Vogt et al. (2002), the mineral assemblage of our aggregate sample was quantified by X-ray diffraction to be 43% calcite, 24% quartz+feldspar, and 20% phyllosilicates (Rabinowitz et al., 2018). Most of the phyllosilicates (8% of the bulk sediment) are mixed-layer clays, with the remaining 12% being an evenly distributed combination of smectite, illite, muscovite, kaolinite and chlorite.

3. Experimental Methods

Our sample was tested as powdered gouge (grain size <125 μm), mixed with 3.5% NaCl brine to form a stiff paste, which we cold-pressed into a sample cell that holds a cylindrical volume of ~20 mm height and 25 mm diameter. We conducted laboratory shear experiments in a single-direct shear device, within which the bottom half of the sample cell is displaced relative to the top half inducing planar shear perpendicular to the cylinder axis (see Ikari, Ito, et al., 2015). The apparatus is equipped with two independent displacement sensors in the shear direction; one mounted at the load cell monitors the apparatus driving (i.e., load point displacement), and one directly at the sample cell measures the true displacement of the sample. Our experiments were conducted at room temperature under fluid-saturated conditions; the sample is confined by the cell and porous metal plates but is not sealed and is allowed to communicate with the pore fluid reservoir. Under application of the normal stress, we allowed the sample to consolidate and drain to the open atmosphere for at least 18 hr, until the sample height (~15–20 mm) reached a steady value. Therefore, although we do not directly measure pore pressure we assume that the sample is drained before shearing and that the applied normal stress is the effective normal stress ($\sigma_n'$).

We sheared our sample under $\sigma_n'$ ranging from 1 up to 15 MPa, the in situ conditions for shallow slow slip at 0.2–3 km depth assuming a vertical effective stress gradient of ~5 MPa/km. Our stress gradient assumes fluid pressure in excess of hydrostatic, as is thought to occur at the northern Hikurangi margin (Bell et al., 2010; Ellis et al., 2015) and in other shallow SSE regions (Kitajima & Saffer, 2012; Saffer & Wallace, 2015). At each effective normal stress, we continuously recorded the shear strength ($\tau$) and calculate the (apparent) coefficient of sliding friction as $\mu = \tau / \sigma_n'$. We sheared the sample at a constant displacement (or slip) rate $V$ of 10 μm/s for up to ~4–5 mm, then decreased the driving rate to 1.7 mm/s (5 cm/yr) for ~2 mm to simulate naturally slow plate tectonic driving rates (Figure 2). We measure the stress drop, event slip, peak slip velocity, and unloading stiffness for the laboratory SSEs generated during the plate rate experiments. The driving velocity was then increased to 5.1 mm/s to measure the rate- and state-dependence of friction (RSF) using established inverse modeling techniques (Ikari et al., 2009; Reinen & Weeks, 1993; Saffer & Marone, 2003) (Figure 2).

The frictional response to a velocity step is described by the following relations:
\[
\mu = \mu_0 + a \ln \left( \frac{V}{V_0} \right) + b_1 \ln \left( \frac{V_0 \theta_1}{d_1} \right) + b_2 \ln \left( \frac{V_0 \theta_2}{d_2} \right),
\]

(1)

\[
\frac{d\theta_i}{dt} = 1 - \frac{V \theta_i}{d_i}, \quad i = 1, 2
\]

(2)

where \(a, b_1, \) and \(b_2\) are dimensionless constants, \(\theta_1\) and \(\theta_2\) are state variables (units of time), and \(d_1\) and \(d_2\) are critical slip distances over which friction evolves to a new steady state value (e.g., Dieterich, 1979, 1981; Marone, 1998; Scholz, 2002). One or two state variables may be used to describe the data as necessary.

Equation (2) describes the time-dependent evolution of the state variable \(\theta\) and is known as the “Dieterich” or “slowness” law, which has the property that friction can change as a function of time and not only slip. Another well-known law used to describe the evolution of the state variable dictates that friction can change only if slip occurs and, accordingly, is called the slip law (Ruina, 1983). For certain cases such as large velocity perturbations, some studies show that the slip law better describes laboratory data (e.g., Bhattacharya et al., 2015), but for the small velocity increases we employ here that the two laws provide nearly identical results. For both state evolution laws, at steady state \(d\theta/dt = 0\) and equations (1) and (2) simplify to
\[ a - b = \frac{\Delta \mu_s}{\Delta \ln V}, \quad (3) \]

where \( \mu_s \) is a steady-state value of friction and \( b = b_1 + b_2 \). A negative value of \( a - b \) corresponds to velocity-weakening friction and indicates the possibility of unstable slip, whereas materials exhibiting positive \( a - b \) values (or velocity-strengthening friction) are expected to slide stably (e.g., Dieterich, 1986; Dieterich & Kilgore, 1996; Scholz, 1998).

The occurrence of unstable slip, which results in earthquakes in nature and stick-slip behavior in the laboratory, depends on a competition between the unloading stiffness (stress drop/slip) of the fault \( K_c \) and the elastic stiffness of the surroundings \( K \), where \( K \) is the stiffness of the testing apparatus (or host rock in nature) (Cook, 1981). If the stress is relieved faster on the fault compared to its surroundings (i.e., \( K < K_c \)), an energy imbalance will occur which drives the slip instability (Dieterich, 1986; Dieterich & Kilgore, 1996; Rice & Ruina, 1983; Scholz, 1998, 2002). \( K_c \) is determined from RSF parameters, although we will later discuss an alternative method for determining \( K_c \). In terms of RSF parameters, the condition for slip instability is (Gu et al., 1984)

\[ K < K_c = \frac{(b-a)\sigma_n}{d_c}. \quad (4) \]

For simplicity, we assume that \( d_c = d_{c1} \) from equations (1) and (2). It can be seen from equation (4) that a velocity-strengthening material (where \( b - a < 0 \)) makes the condition \( K < K_c \) impossible, so that instability should not occur.

Equation (4) is the criterion for true slip instability, defined as the ability for the slip velocity to accelerate uninhibited toward infinity (e.g., Dieterich, 1986; Ruina, 1983). However, the RSF formulation using the Dieterich evolution law can also produce accelerating slip in velocity-strengthening materials, although it cannot continue to infinity. In this case, the critical stiffness criterion is

\[ K < K_b = \frac{b\sigma_n}{d_c} + \frac{T}{V_i}. \quad (5) \]

where \( T \) is an external shear stressing rate \( d\tau/dt \) and \( V_i \) is the initial slip velocity (Dieterich, 1992). Assuming that the external stressing rate \( T \) is zero (i.e., the shear stress on the fault is approximately constant), it can be seen that this criterion is similar to the criterion for full instability, but with the critical stiffness depending on the parameter \( b \) rather than \( a - b \). As noted by Dieterich (1992), instabilities nucleating according to this criterion may be expected to have quite limited slip, because the velocity-strengthening property will tend to damp the instability and stabilize slip. The second term on the right-hand side of equation (5) also suggests that external stress perturbations could be an important triggering mechanism especially since initial slip rates can be quite low, but we do not investigate this further in this study.

The stiffness \( K \) of our apparatus was measured by loading a steel blank the same size as our samples at a rate of 5 kPa/s under 1, 5, 10, and 15 MPa normal load, up to shear loads corresponding to a friction coefficient of at least 0.6 (well exceeding the range of friction coefficients in this study). For the observations in this study, stiffness values which matched the relevant testing conditions range from ~2–9 MPa/mm depending on the normal and shear loads. We use a critical stiffness analysis to test whether the characteristics of laboratory SSEs are consistent with the classification as frictional instabilities, and furthermore how well laboratory tests (i.e., velocity-step tests) can predict such behavior.

### 4. Observations From Laboratory Friction Experiments

#### 4.1. Laboratory SSEs

The steady-state friction coefficient of the Hikurangi sediment is consistently 0.36–0.43 at the initial slip rate of 10 \( \mu \)m/s, and 0.41–0.45 at the slow rate of 1.7 nm/s over all effective normal stresses in this study. In five of our seven experiments, we observe 2–3 SSEs which appear spontaneously during the ~2 mm of sliding under plate-rate driving at 1.7 nm/s (Figure 2 and supporting information). Laboratory SSEs were observed at each effective normal stress in this study (Figure 2). In general, the laboratory SSEs exhibit the following...
characteristics: upon initial shearing at the driving rate, the shear stress increases signifying partial locking and slip deficit accumulation. This is followed by a stress drop of roughly equal magnitude to the loading and a simultaneous increase in sample slip rate above the programmed driving rate (i.e., sample displacement minus load point displacement), which we identify as the SSE itself. In some (but not all) SSEs, there is a phase of significant steady or quasi steady state slip between the loading phase and stress drop (Figure 2). After the SSE stress drop, the slip rate returns to the driving rate.

In Figure 3, we compare a geodetically detected natural SSE from the northern Hikurangi margin with a laboratory SSE. Shown as an example is the cGPS position record from station GISB during the 2014 Gisborne SSE (Wallace et al., 2016). Between SSEs, the time series shows a general westward motion along the direction of Pacific Plate subduction, indicating locking (or partial locking) between the plates along the subduction interface. The sudden reversal to eastward motion signifies the SSE, with a maximum of ~25 cm of slip estimated on the plate boundary fault during this particular event (Wallace et al., 2016). The form of the surface deformation response recorded by the cGPS site is very similar to the excess slip measured in laboratory SSEs, here depicted as the difference between the sample displacement and the load point displacement. Both the natural and laboratory SSEs show a trend of accumulating slip deficit before the slip event, a relatively sudden accumulation of slip, and a return to slip deficit accumulation following the event.
point of difference to note in Figure 3c is that for the Gisborne SSE, the total slip on the plate boundary (at the point of maximum slip) is shown, whereas the slip in the laboratory SSE in Figure 3e is the excess slip (e.g., the slip beyond the steady plate motion rate). It is also important to note that the plate boundary prior to the 2014 Gisborne SSE is mostly locked and accumulating strain at nearly the full plate motion rate, whereas the sample prior to the laboratory SSE is deforming at roughly half the driving rate.

Although slip and slip velocity during the stress drop portion of the laboratory SSEs is strikingly similar to the cGPS records of natural Hikurangi SSEs (compare Figures 3a and 3e), there are also some clear differences. One is the regular, repetitive nature of the natural SSEs, which is not established in these laboratory experiments. Another difference is the steady shearing at the driving rate in the experiments, which occurs before the loadup and after the stress drop, and sometimes between the loadup and stress drop. Because such a large amount of steady shearing may not be representative of some natural slow slip faults (many of which relock quickly after an SSE, with little to no slip between SSEs), the key parameters from the laboratory SSEs (stress drop, duration, peak slip velocity, slip, and unloading stiffness) were measured specifically from the stress drop portion of the laboratory SSE. This is the part of the experimental data which most closely resemble natural SSE slip behavior (Figure 3).

For our complete set of laboratory SSEs, we observe stress drops in the range 8–100 kPa, durations of ~0.5–1.5 hr, peak slip velocities in the range 8–19 cm/yr, velocity increases (as quantified by $V/V_o$) of 1.5–5.3, and event slip of 2–20 μm (Figure 4, Table 3). Despite some instances of significant scatter, the stress drop, duration, peak slip velocity, slip velocity increase, and event slip all generally increase as a function of increasing effective normal stress (Figure 4). Other measurable parameters such as percent stress drop, steady-state slip preceding the stress drop, and absolute strengths prior to and after the stress drop do not show recognizable patterns as a function of effective normal stress (see supporting information).

4.2. Velocity-Dependent Frictional Behavior

From our velocity step tests for which velocity is increased from the plate rate of 1.7 nm/s, we observe velocity-weakening friction ($a − b$) of $−0.0019$ to $−0.0003$ at all effective normal stresses with the exception of 5 MPa ($a − b = 0.0006$) (Figure 5). RSF parameters obtained from velocity step tests can be used to guide expectation of slow or fast slip behavior via the critical stiffness criterion (equation (4)) (e.g., Ikari, Trütner, et al., 2015; Niemeijer & Vissers, 2014; Trippetta et al., 2017). An important, but subtle point to consider is that equation (4) uses the parameter $a − b$, which includes a term for the velocity change (equation (3)). Therefore, this critical stiffness criterion is specifically applicable to the velocity changes employed in the
velocity step test, which in our case is $V/V_o = 3$. However, direct measurement of the velocity change during our laboratory SSE reveals $V/V_o$ of 1.5–5.3 (Table 3). In order to directly compare $K_c$ and $K/K_c$ values from laboratory SSEs with $K_c$ and $K/K_c$ values calculated from RSF parameters, we multiply equation (4) by $\Delta \ln V_{SSE}$, which describes the change in slip rate during laboratory SSEs. We also use this factor to calculate $K/K_b$, the criterion for accelerating stable slip. Note that the critical slip distance $d_c$ is implicitly assumed to be unaffected by variations in the velocity change. Since we use threefold increases in velocity for each of our velocity step tests, we cannot evaluate the effect of velocity increase magnitude on $d_c$. However, recent experiments using a clay-bearing synthetic gouge suggest that for velocity steps conducted at $\leq 1$ mm/s, $d_c$ does not vary greatly for velocity changes of up to 4 orders of magnitude (Ito & Ikari, 2015).

### Table 3
Experimental SSE parameters

| Experiment | Effective Normal Stress (MPa) | Stress Drop (kPa) | Event Slip (mm) | Initial Velocity (cm/yr) | Initial Slip Velocity (cm/yr) | Peak Velocity (cm/yr) | Peak Slip V | Event D/r | Apparatus Stiffness K (MPa/mm) | SSE Stiffness Ks (MPa/mm) | Unloading Kc (MPa/mm) | $K_c$ Unloading Stiffness Ks (MPa/mm) |
|------------|-------------------------------|-------------------|-----------------|-------------------------|-------------------------------|----------------------|------------|-----------|--------------------------------|------------------------|-------------------|----------------------------------|
| B659       | 1                             | 8.3               | 4.3             | 6.0                     | 9.2                           | 1.5                  | 3.4E-04    | 8.2       | 2.2                             | 1.0                    | 2.2                | 1.0                              |
| B659       | 1                             | 8.3               | 2.0             | 4.7                     | 7.5                           | 1.6                  | 1.5E-04    | 8.9       | 3.5                             | 0.7                    | 3.5                | 0.7                              |
| B669       | 5                             | 23.2              | 10.1            | 7.6                     | 12.6                          | 1.7                  | 7.9E-04    | 2.3       | 2.8                             | 2.2                    | 2.8                | 2.2                              |
| B669       | 5                             | 32.2              | 9.0             | 4.4                     | 12.8                          | 2.9                  | 7.1E-04    | 2.4       | 4.5                             | 1.5                    | 4.5                | 1.5                              |
| B628       | 10                            | 22.7              | 16.5            | 2.8                     | 14.9                          | 5.3                  | 1.3E-03    | 9.1       | 2.5                             | 3.2                    | 2.5                | 3.2                              |
| B628       | 10                            | 22.8              | 13.5            | 4.8                     | 14.2                          | 2.9                  | 1.1E-03    | 8.7       | 2.5                             | 3.6                    | 2.5                | 3.6                              |
| B678       | 10                            | 35.7              | 5.8             | 5.3                     | 18.7                          | 3.5                  | 4.5E-04    | 6.3       | 13.7                            | 0.7                    | 13.7               | 0.7                              |
| B678       | 10                            | 29.9              | 11.2            | 4.7                     | 19.3                          | 4.1                  | 8.8E-04    | 6.5       | 3.1                             | 2.9                    | 3.1                | 2.9                              |
| B678       | 10                            | 44.5              | 11.8            | 4.3                     | 11.6                          | 2.7                  | 9.3E-04    | 8.9       | 8.0                             | 1.1                    | 8.0                | 1.1                              |
| B668       | 15                            | 99.9              | 19.6            | 4.7                     | 16.0                          | 3.4                  | 1.5E-03    | 8.9       | 8.2                             | 1.1                    | 8.2                | 1.1                              |
| B668       | 15                            | 80.3              | 18.2            | 4.8                     | 15.4                          | 3.2                  | 1.4E-03    | 8.9       | 7.8                             | 1.1                    | 7.8                | 1.1                              |

$r = 12.7$ mm
$V_o = $ initial slip velocity (cm/yr), $r = $ sample radius (mm)

**Figure 5.** (a) Velocity-dependence of friction $\alpha$-$b$, (b) critical stiffnesses $K_c$, $K_b$, and $K_s$, and (c) stiffness ratios $K_c/K_s$, $K_b/K_s$, and $K/K_s$ as a function of effective normal stress. $K_c$ is either measured directly from the slope of the stress versus displacement record during laboratory SSE (black circles), or calculated from velocity step data (blue triangles). Apparatus stiffness $K = 2–9$ MPa/mm (see Table 3).
The values of $K_c$ that we obtain from our velocity step data and equation (4) range from 0.5 to 2.6 MPa/mm; $K_b$ values are consistently larger and range from 1.1 to 5.9 MPa/mm (Figure 5). Neither $K_c$ nor $K_b$ exhibit a dependency on effective normal stress. For the experiment conducted at 5 MPa, $K_c$ is a physically impossible negative value due to a measured positive $a - b$ value; $K_b$ values, on the other hand, can be calculated and evaluated. The stiffness of our apparatus $K$ increases as a function of both normal and shear load. We picked $K$ values from the loading curves to match our experimental conditions; these values range from ~2–9 MPa/mm resulting in $K/K_b$ values ranging from 3.4–6.8. $K/K_b$ values are smaller and range from 1.2–4.3. Although the $K/K_b$ values are smaller and approach 1, values <1 are not observed which indicates a frictionally stable material (Figure 5).

Because we observe SSEs with clear stress drops in our laboratory experiments, we can also evaluate the sample critical stiffness directly by measuring the slope of the shear stress-displacement record during the SSE stress drop (e.g., Figure 2c). We interpret the maximum value to be a directly-measured critical stiffness during an SSE, which we call $K_c$. $K_c$ values range from 2.2–13.7 MPa/mm and result in $K/K_b$ ranging from 0.7–3.6, with about half of the $K/K_b$ values near or below 1 (Figure 5). $K_c$ increases slightly as a function of effective normal stress, although this trend is obscured by some scatter at 10 MPa. $K/K_c$ does not show a dependence on normal stress, because the slight trend in $K_c$ is canceled out by the normal stress dependence of $K$.

5. Comparison of Natural and Laboratory SSEs

We now compare the characteristics of our laboratory-observed SSE with a catalog of 19 shallow and 12 deep natural SSEs observed in the Hikurangi subduction zone (Wallace et al., 2009, 2012, 2016, 2017; Wallace & Beavan, 2006, 2010; Wallace & Eberhart-Phillips, 2013) (Tables 1 and 2). We compile estimates of slip magnitude, duration, depth, slip dimensions, slip rate, moment release, and stress drop based on results of these previously published geodetic studies of Hikurangi SSEs (Tables 1 and 2). Total slip, slip velocity, and duration are extracted directly from the GPS data. Natural SSE stress drop ($\Delta \tau$) is estimated following the energy-based approach of Noda et al. (2013), which is a robust way to obtain stress drop for models with distributed slip. To do this, shear stress change is calculated for each patch/subfault in each of the SSE slip models using the equations of Okada (1992). The energy-based stress drop (Noda et al., 2013) can be expressed as:

$$\Delta \tau = \frac{\sum_{i=1}^{N} \Delta \tau_i u_i}{\sum_{i=1}^{N} u_i},$$

where $\Delta \tau_i$ and $u_i$ are the stress drop (i.e., shear stress change) and slip amounts, respectively, for each slipping patch, $i$. The natural SSEs have an equivalent $M_w$ of ~6–7, assuming $G = 10$ GPa for the shallow SSEs (Table 1), and $G = 30$ GPa for the deep SSEs (Table 2), which is consistent with shear moduli estimated for these depths from global subduction earthquakes (Bilek & Lay, 1999; Geist & Bilek, 2001). We note that the estimated moment magnitudes for the shallow SSEs in Table 1 are lower than those published previously, as those studies assumed a shear modulus of 30 GPa (e.g., Wallace et al., 2012, 2016; Wallace & Beavan, 2010; Wallace & Eberhart-Phillips, 2013).

To estimate the effective normal stress in the SSE source regions we assume moderate fluid overpressure approximately halfway between hydrostatic and lithostatic, for an effective normal stress gradient of 5 MPa/km. This assumption is based on seismic reflection data indicating significantly elevated fluid pressures within the Hikurangi slow slip region (Basset et al., 2014; Bell et al., 2010). Our range of effective normal stress for the experimental SSEs therefore projects to 0.2–3 km depth, which spans the upper region of slip in the shallow SSE area (e.g., Wallace et al., 2016). Although our laboratory experiments were conducted at effective normal stresses that correspond to much shallower depths than the Hikurangi SSEs, the increasing trends with effective normal stress we observe facilitate extrapolation of laboratory-measured SSE parameters to deeper depths. For these extrapolations we use linear and power law fits to the laboratory-measured quantities, which exhibit coefficient of determination $R^2$ ranging from 0.54–0.75.

The stress drops of 8–100 kPa that we observe in our experiments are comparable to but slightly higher than the stress drops of 1–52 kPa observed for shallow SSEs, and very similar to the 23–129 kPa stress drops observed for the deep SSEs (Figure 6). The observation that the deeper Hikurangi SSEs have larger stress...
drops than the shallow SSEs is generally consistent with expectations from our laboratory data set; however, the projections overestimate the absolute stress drop values at depth. The peak slip velocities of shallow SSEs at the northern Hikurangi range from 73–1147 cm/yr (0.2–3.1 cm/day), significantly faster than both our laboratory events (8–16 cm/yr, or 0.02–0.04 cm/day), and also deep SSEs at southern Hikurangi (12–164 cm/yr or 0.03–0.45 cm/day). The shallow Hikurangi SSEs are faster than the deeper SSEs, in contrast with expectations from the laboratory SSEs. Interestingly, the depth-extrapolated peak slip velocities from the laboratory SSEs provide a good match to the deep Hikurangi SSEs (Figure 6). On the Hikurangi subduction interface the inter-SSE slip rate varies spatially and sometimes temporally, but is estimated to range from 0 (fully locked) to 3 cm/yr in the north, and 0 to 2 cm/yr in the south (Wallace & Beavan, 2010). Taking inter-SSE slip rates of 2.0 cm/yr in the northern Hikurangi and 1.5 cm/yr in the southern Hikurangi as representative, the ratio of slip velocity increase \( V/V_0 \) ranges from 36 to 574 in the northern Hikurangi and 8 to 110 in the southern Hikurangi. This is significantly larger than both the twofold to fivefold increases in slip velocity measured in the laboratory SSEs, although the low values in the southern Hikurangi approach the laboratory values.

The duration of the shallow SSEs ranges from 7–34 days, and the total durations of deep events range from >300–550 days (with subevents of 60 days or more). Although the combined data set shows a trend of

Figure 6. Comparison of parameters from laboratory SSEs with natural shallow (northern Hikurangi) and deep (southern Hikurangi) SSEs as a function of depth: (a) stress drop, (b) peak slip velocity, (c) duration, (d) event slip, and (e) slip/length ratio \( D/r \). Effective stress gradient is assumed to be 5 MPa/km. See text for more details on SSE parameters. Linear and power law fits to the laboratory data are extrapolated to 60 km depth.
increasing duration with depth as indicated by the laboratory SSEs, the durations of natural SSEs are ~2 orders of magnitude longer than the projections from the experiments (Figure 6). The maximum event slip is similar for both shallow and deep natural SSEs and ranges from ~30–300 mm. All of the natural SSEs have slip amounts that are orders of magnitude larger than those in laboratory experiments, both in terms of absolute values and the values projected to higher effective normal stresses. In order to compare between the laboratory SSEs which occur on a 500 mm² surface and natural SSEs with rupture dimensions of thousands of km², we use the dimensionless ratio $D/r$, where $D$ is the maximum event slip and $r$ is the patch half length in the slip direction (Chinnery, 1969; Dieterich, 1986). We observe that both shallow and deep SSEs have similar $D/r$ ratios, with most values ranging from $10^{-7}$ to $10^{-6}$. These values are approximately 2 orders of magnitude smaller than laboratory values of $D/r$, and approximately 3 orders of magnitude larger than the depth projections of $D/r$.

6. Discussion

6.1. Mechanism of Laboratory SSEs

The physical mechanisms of SSE generation are generally not well known, but SSEs can be numerically simulated by implementing velocity-weakening faults that are very close to the condition of “neutral stability” (e.g., Liu & Rice, 2005, 2007; Rubin, 2008), which is the boundary between stable sliding and unstable slip where self-sustained “stable” oscillatory motion may occur (Dieterich, 1986; Ruina, 1983; Scholz, 1998). Laboratory studies support this idea, showing that $K = K_c$, or $K$ slightly smaller than $K_c$ is a condition favorable for oscillatory slip that may represent SSEs (Leeman et al., 2016; Scuderi et al., 2016). Two-dimensional RSF models suggest that in order for slow slip patches to grow to the size observed in subduction zones (without overtuning of RSF parameters), additional processes are needed. One popular mechanism is an observed transition in $a \rightarrow b$ from velocity weakening to velocity strengthening with increasing slip velocity, used as a mathematical cutoff that limits the slip rate (i.e., cutoff velocity) (e.g., Matsuzawa et al., 2010; Shibazaki & Iio, 2003; Shibazaki & Shimamoto, 2007). Other mechanisms for keeping slip instabilities slow include dilatancy hardening, in which dilatancy during slip causes a drop in pore pressure that strengthens the fault (Rubin, 2008; Segall et al., 2010), and geologic heterogeneity causing a distribution of velocity-weakening and velocity-strengthening fault patches (Skarbek et al., 2012). Despite the difference in mechanisms limiting the event velocity, common to all these is an initially nucleating instability at the condition $K/K_c < 1$ and propagation of an SSE within the rupture patch.

The $K/K_c$ values calculated from velocity step data all exceed 1, indicating that the criterion for slip instability is not satisfied. On the other hand, many of the $K/K_c$ values obtained from the SSE stress drops are near or sometimes below 1. Since $K_c$ is directly measured from the SSE stress drop it is difficult to associate it with a mechanism. We note that $K_c$ and $K/K_c$ are more similar to the values of $K_b$ and $K/K_b$, than they are to $K_c$ and $K/K_c$ (Figure 5). This suggests that the laboratory SSEs may be instances of accelerating stable slip. Dieterich (1992) noted that accelerating slip arising from satisfying equation (5) can occur for velocity-strengthening materials, where the velocity-strengthening property functions as a slip stabilizer. This is consistent with studies utilizing a critical slip rate above which velocity-weakening friction limits the event slip velocity. Recently, friction experiments conducted at 10 MPa effective normal stress have shown that the transition velocity for the same Hikurangi samples we use here is ~1 μm/s (Rabinowitz et al., 2018). Most of the peak slip velocities we observe (both in natural and laboratory SSEs) are at least an order of magnitude lower than 1 μm/s, perhaps suggesting that the cutoff velocity alone is unlikely to be the mechanism for Hikurangi SSEs. However, accelerating slip depends on whether the critical stiffness criterion (equation (5)) is satisfied, not necessarily if velocity-strengthening occurs. Therefore, the effect of a 1 μm/s transition velocity may be to limit natural SSEs to a maximum slip rate of ~0.1–0.4 μm/s. This inference is consistent with numerical simulations of SSEs using a 1 μm/s cutoff velocity, which show that the SSE peak slip velocities are near or sometimes lower than the cutoff velocity (Hawthorne & Rubin, 2013; Shibazaki & Shimamoto, 2007), but would need to be verified specifically for the Hikurangi margin. We emphasize that this transition velocity has thus far only been measured at 10 MPa effective normal stress on the Hikurangi samples; however, we also note that while $K/K_b$ values approach 1, values less than 1 are not observed.

The observation of laboratory SSEs despite the critical stiffness criteria $K/K_c$ and $K/K_b$ not being satisfied indicates that $K_c$ values measured directly from laboratory SSEs may be a more reliable indicator of slow
slip behavior compared to RSF parameters extracted from velocity-step data, especially in material with $a - b$ values that are positive or near 0. A similar approach was used by Harbord et al. (2017), who used stiffness values from stick-slip stress drops to reconcile the appearance of stick-slip in a velocity-strengthening material. Furthermore, although $K/K_b$ values >1 nominally indicate stable frictional behavior, we note that it is not established what range of $K/K_b$ values allow slow slip, that is, how close $K/K_b$ must be to 1. Our data, which show that $K/K_b$ from laboratory SSEs is mostly < ~3, suggest that slow events can be generated when $K/K_b$ is slightly positive. In experiments using quartz powder in which the critical stiffness was controlled by adjusting the effective normal stress, Scuderi et al. (2016) and Leeman et al. (2016) observed that slow stick-slip mostly occurred when $K/K_c$ ≤ 1, but some events occurred for $K/K_c$ up to 1.2. Their experiments therefore demonstrate that slip instability can occur even when the critical stiffness criterion is not satisfied, which we suggest may also be the case for stable accelerating slip via low $K/K_b$.

6.2. Differences Between Laboratory and Natural SSEs

In comparing the laboratory and natural Hikurangi SSEs, we have largely focused on SSE parameters measured during the peak slipping, or stress drop phase of the laboratory SSEs, which bear strong similarities to cGPS observations of the natural Hikurangi SSEs. However, other aspects of the laboratory SSEs are not consistent with natural SSEs. These include the steady shearing (sample slip rate about the same as the driving rate) before loadup, after the stress drop, and sometimes between the loadup and stress drop; the lack of regular recurrence of the laboratory SSEs; the spontaneous nature of partial locking represented by the loadup phase; and the short duration of the partial locking compared to steady shearing. Wallace and Beavan (2010) determined an inter-SSE locking distribution for the Hikurangi subduction interface, and the slip deficit rates in the shallow, northern Hikurangi SSE region range from 2–5 cm/yr, roughly corresponding to an inter-SSE slip rate in the SSE source of 0–3 cm/yr (where 0 is fully locked). In natural SSEs at north Hikurangi, fault locking appears to resume within a few weeks of the SSEs, and the SSE source regions there appear to largely maintain this coupling until the next SSE.

The occurrence of $K/K_b$ > 1 in our experiments indicates a tendency for stable slip that could partially explain the steady shearing (sample slip rate about the same as the driving rate) before and after the stress drop, and also the lack of regular recurrence of the laboratory SSEs. We speculate that perhaps a lower $K/K_b$, whether from lower apparatus stiffness, higher normal load, or smaller $d_c$ could result in more regularly repeating SSEs, larger peak slip velocities, and lower inter-SSE slip velocities that more closely resemble natural SSEs. The steady shearing before the load-up phase also indicates that our samples experience spontaneous partial locking, which is likely facilitated by the extremely low driving rates we employ here. Slow shearing may allow time-dependent frictional healing (e.g., Dieterich, 1972) to become significant even during shear, which has been suggested to favor velocity-weakening friction at low slip rates (Ikari & Kopf, 2017).

Another potentially important factor may be the role of the critical slip distance $d_c$. Scaling $d_c$ from the laboratory to the field is a long-standing and nontrivial problem, largely due to uncertainty as to what it physically represents (e.g., Dieterich, 1981; Griffith & Prakash, 2015; Marone & Kilgore, 1993; McLaskey & Kilgore, 2013). A relevant observation is that following the 10 μm/s run-in, at least 0.6 mm of sliding at the plate rate is required before the laboratory SSEs begin to occur. This might suggest that the spontaneous partial locking leading up to the laboratory SSEs requires attainment of a steady-state microstructure or surface roughness. We speculate that this microstructure or roughness could be characterized by a specific $d_c$ value (e.g., Candela & Brodsky, 2016). As seen in equation (4), smaller $d_c$ favors instability by increasing $K_c$. Although the evolution of $d_c$ may play a significant role, it is subject to difficulties in scaling and will need to be addressed in a future study.

We also note that other processes not replicated in our experiments may play a role in contributing to relocking processes observed between natural SSEs from cGPS. For example, temporal variations in fluid pressure in the fault zone due to fault-valve behavior (Sibson, 1990) during the SSE cycle could influence the timing of relocking following the SSE. Other natural processes occurring within the fault zone, such as silica dissolution, diffusion, and precipitation (Fisher & Brantley, 2014), or pressure solution (Rutter, 1983; Yasuhara et al., 2005) may also influence the relocking phase observed geodetically. Relocking, and temporal
variations in locking rate observed geodetically could also be explained by the development of force chains between clasts in the mélange/shear zone of plate boundary faults (e.g., Beall et al., 2019).

### 6.3. Implications for Hikurangi SSE Environment

Our laboratory SSEs exhibit overall depth-increasing trends in parameters such as stress drop, peak slip velocity, event duration, slip, and slip per patch length (Figures 4 and 6). This is consistent with critical stiffness theory which predicts greater instability, and hence larger events, with increasing effective normal stress (equations (4) and (5)). However, projecting these quantities to the depths at which Hikurangi SSEs are observed does not match the observations. An intriguing exception can be seen for the peak slip velocity, where the projections from our laboratory data match the observed peak slip velocities for deep SSEs in the southern Hikurangi margin (Figure 6). One interpretation is that the effective stress conditions at these depths are reasonably close to the 5 MPa/km we assume and that the frictional behavior is accurately captured in our experiments (requiring near-lithostatic fluid pressure), although coincidence cannot be ruled out.

The quantities which show the largest difference between the observations and the laboratory projections are the duration, slip and $D/r$. One obvious explanation for the inconsistency in duration and slip is the limited slip in laboratory experiments due to the small size of the samples, for which $r$ is 12.7 mm. The difference in $D/r$ is more difficult to explain, because it is a normalized value, showing that even though the slip in our laboratory experiments is small relative to natural SSEs, the slip per patch size is roughly 3 orders of magnitude larger than that of the natural SSEs. Scaling from the laboratory to nature is an issue (e.g., McClaskey & Kilgore, 2013) because $D/r$ values calculated for the laboratory SSEs use an $r$ value equivalent to, and therefore limited by, the sample radius. One key difference between laboratory and natural SSEs is that the slip distribution in our experiments is essentially a boxcar function, where slip is the same everywhere on the sample but drops to zero at the sample boundaries. Future experiments on larger samples where the slipping patch is allowed to grow without being limited by the small sample size could improve estimates of $D/r$ values for laboratory SSEs.

The small sample size in laboratory experiments also causes difficulty in evaluating the role of heterogeneity, which numerical studies show can be an important factor for SSEs (e.g., Skarbek et al., 2012). In particular, we assume shear moduli of 30 GPa for the deep Hikurangi SSEs and 10 GPa for the shallow SSEs as average values. However, Williams and Wallace (2015, 2018) used recent New Zealand-wide seismic velocity models to incorporate the effects of more realistic heterogeneous elastic properties on SSE slip and slip distribution. They found that that slip (and seismic potency) during shallow Hikurangi SSEs could be underestimated by up to ~40%, in models that assume a uniform, elastic half-space. Assuming that the unloading stiffness during the SSEs is unchanged, this suggests that the natural shallow SSEs stress drops listed in Table 1 may also be underestimated. As applied to our comparisons between extrapolations from laboratory data and natural Hikurangi SSE parameters (Figure 6), considering effects of elastic heterogeneity would reduce the difference between our projections and the shallow Hikurangi stress drops. The difference in the absolute value of slip would increase, but the normalized slip $D/r$ for the shallow Hikurangi SSEs would be closer to the laboratory projections. For the deep Hikurangi SSEs, incorporation of heterogeneous material properties suggests that slip and stress drop are overestimated by elastic half-space models by up to 20% (Williams & Wallace, 2015), and therefore, the effect of using models with uniform elastic properties to obtain stress drop for deep SSEs (Table 2) would be the opposite (but smaller) compared to the effect on the shallow SSEs.

Other considerations that likely have an effect on comparing laboratory and natural SSE parameters include differences in temperature between the shallow and deep SSEs, and limited sample material available for testing. Rabinowitz et al. (2018) found that temperature in the range of the shallow SSEs has little influence on the slip behavior of the Hikurangi sample we study here. However, above temperatures of 110 °C (the limit of their study) we expect temperature to modify rate-and-state friction parameters via diagenesis and low-grade metamorphic processes, and activation of different deformation mechanisms that may operate under different timescales (e.g., Blanpied et al., 1998; den Hartog et al., 2012; Niemeijer & Vissers, 2014).

Although our sample is representative of the majority of the sediment column drilled at Site 1124, it is not yet clear if this interval is representative of the megathrust zone where the SSEs occur. Moreover, our laboratory experiments do not capture the effects of several important factors such as temperature, elevated pore
pressure, specific structure (e.g., microfabrics), and spatial heterogeneities in lithology. However, coring of the sedimentary section on the subducting Pacific Plate just seaward of the deformation front, a main active frontal thrust, and the upper portion of the overriding plate was carried out during IODP Expedition 375 (Wallace et al., 2019). Logging-while-drilling data acquired during IODP Expedition 372 will further help characterize the ambient conditions and rock properties at the prism toe and within the incoming sedimentary section (Wallace et al., 2019). The samples and data obtained from these two cruises will be critical to constrain the relationship between laboratory and geodetic observations of SSEs. Observatories installed during these expeditions will also give us tighter constraints on the slip rate characteristics of offshore north Hikurangi SSEs in the future.

7. Summary and Conclusions

We performed ultraslow laboratory friction experiments utilizing plate tectonic driving rates (5 cm/yr), which produced laboratory SSEs. Our laboratory SSEs exhibit some key similarities with natural SSEs observed in the Hikurangi subduction zone offshore the North Island of New Zealand, including the form of the displacement record and the size of the stress drop. Using friction parameters measured from velocity step tests, we find that the critical stiffness criterion for unstable slip (based on the parameter \( a - b \)) is not satisfied. A similar criterion for stable accelerating slip (based on the parameter \( b \)) suggests that SSEs may occur in the nominally “stable” regime, where \( K/K_b < -4 \). Critical stiffness measured directly from laboratory SSE stress drops appears to be a better predictor of fault behavior than stiffness parameters extracted from velocity-step tests in laboratory experiments.

The laboratory SSEs exhibit increasing stress drop, duration, peak slip velocity, slip velocity increase, and total slip as a function of increasing effective normal stress. We use this dependence on effective normal stress to extrapolate these quantities to the depths of naturally occurring Hikurangi SSEs. Comparing the projections with a comprehensive catalog of SSEs documented at the Hikurangi margin shows that, with the exception of the peak slip velocity of deep southern Hikurangi SSEs, the projections fail to match the observations. This highlights difficulties scaling laboratory experiments to field observations, and that correlation between laboratory and natural SSEs is not completely straightforward. This latter point can be improved by further work using new data and samples from recent scientific drilling in the Hikurangi subduction zone.

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