Dynamic mitigation of tearing mode instability in current sheet in collisionless plasma

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Dynamic mitigation for the tearing mode instability in the current sheet in collisionless plasma is demonstrated by applying a wobbling electron current beam. The initial small amplitude modulations imposed on the current sheet induce the electric current filamentation and the reconnection of the magnetic field lines. When the wobbling or oscillation motion is added from the electron beam having a form of a thin layer moving along the current sheet, the perturbation phase is mixed and consequently the instability growth is saturated remarkably, like in the case of the feed-forward control.

The dynamic mitigation of plasma and fluid instability was proposed in Refs. [1–4]. This approach uses the superimposing the phase-controlled plasma perturbations with the modulations growing due to the instability developing. As a result the instability growth reduces, like in the case of the feed-forward control [5, 6], by an energy-carrying driver introducing perturbations into plasma systems parameters. If the perturbation phase is controlled by, for example, wobbling motion of driver beam, the superimposed overall perturbation amplitude can be saturated.

Here with the particle-in-cell simulations, we demonstrate the dynamic mitigation of the tearing mode instability of the current sheet in collisionless plasma. Theory and 3-dimensional (3-D) simulations show a clear mitigation of the electron current filamentation growth studied in Refs.[7–11] corresponding to the magnetic reconnection [12–22]. A current sheet in a plasma creates an anti-parallel magnetic field with a magnetic changing the sign in the electron current sheet as shown in Fig. 1(a). Rising up the tearing mode instability results in the magnetic reconnection.

The current sheet formation in high electric conductivity plasmas can be found in various situations: for example, the magnetic reconnection via the current sheet formation and disruption is considered as a basic mechanism of the solar flares [23], the magnetic reconnection in the current sheets on the day side and in the tail of the earth magnetosphere plays the key role in the high energy charged particle acceleration [24, 25], and the magnetic reconnection is crucially important in developing the controlled magnetic confinement fusion [26, 27]. The magnetic reconnection studies with the high power laser interaction with matter is a fast developing research direction in so-called laboratory astrophysics [28–30].

RESULTS

The equilibrium state for the current sheet in a collisionless plasma based on the Harris solution presented in Ref. [31] is used as an initial configuration in the computer simulations whose results are discussed below. In the case under consideration, the current sheet is located in the y–z plane with electric current directed along the x axis as

FIG. 1: (color online) (a) Schematic of plasma system sustained by electron current sheet. The magnetic reconnection is induced along with the plasma filamentation. The initial conditions of (b) the electron number density $n_e$ and (c) the magnetic field are also presented.
shown in Fig. 1b). According to Ref. [31] the distribution function of the \( j = e, i \) particle species is given by

\[
f_j(v, z) = \frac{n_j}{(2\pi v_{Tj}^2)^{3/2} \cosh^2(z/L)} \exp\left[-\frac{(v_x - v_{Tj})^2 + v_y^2 + v_z^2}{2v_{Tj}^2}\right],
\]

where \( v = (v_x, v_y, v_z) \) (for describing the initial equilibrium we assume a non-relativistic approximation), \( v_{Tj} \) is the thermal velocity of the \( j \) species particle, whose temperatures are given by \( T_j = m_j v_{Tj}^2/2 \). Under the condition

\[
\frac{V_e}{T_e} = -\frac{V_i}{T_i},
\]

the electron density and ion density are equal to each other \( n_e(y) = n_i(y) = n(y) \). For the sake of simplicity we assume that \( T_e = T_i = T \), i.e. \( V_e = -V_i = V \). In this case, the density and magnetic field dependences on the coordinate \( z \) are

\[
n(z) = \frac{n}{\cosh^2(z/L)}
\]

with the maximum of the density at \( z = 0 \) and

\[
B(z) = B_0 \tanh(z/L)e_y,
\]

with \( B_0 = (16\pi nT)^{1/2} \), i.e. the magnetic field changes the sign at \( z = 0 \), and \( e_y \) is the unit vector in the \( y \) direction. The current sheet thickness \( L \) is equal to

\[
L = \frac{c}{V} \left( \frac{T}{4\pi e^2} \right)^{1/2} = \frac{\lambda_D}{\beta}
\]

with \( \lambda_D \) and \( \beta = V/c \) being the Debye length and the electron (ion) average velocity normalized on the speed of light in vacuum, \( c \). Further, the particle in cell simulations are carried out in the frame of reference moving along the \( x \) axis with the normalized velocity equal to \( \beta \). In the boosted frame of reference the ions are at the rest, the electrons move with the velocity \(-2c\beta \), and the electron and ion density are related to each other as \( n_e = n_i + 2\gamma\beta^2 n \). The electric field arising from the electric charge separation is expressed by \( E = \gamma\beta B_0 \tanh(z/L)e_z \), where \( \gamma = 1/\sqrt{1 - \beta^2} \).

The initial small perturbations are imposed on the electron density \( n_e \) along the \( y \) direction. The perturbations are periodic with the amplitude of 5\% and the wavelength of \( L_y = 0.1m \).

In our simulations we employ 3D particle-in-cell EPOCH [32]. The simulation box is \( 0.2 \times 0.2 \times 0.2 m \), and the maximum electron density is \( n_0 = 1.0 \times 10^{14} m^{-3} \). The corresponding mesh cells are \( 200 \times 200 \times 200 \) with 64 particles in each cell. The details of the simulations and the code information are presented in the Methods.

For the chosen electron temperature, 116 keV, and the energy of the electron motion \( m_e c^2 \beta^2/2 \), the scale lengths of the density and magnetic field in the current sheet, \( \lambda_D/\beta \), and of the perturbation wavelength, \( L_y \), in our system are larger than the electron inertial length \( c/\omega_{pe} \), which is equal to the electron Larmor radius \( r_{Be} = m_e v_{Te}/eB_0 \).

Figures 2 show the spatial distributions of the electron number density \( n_e \) at \( t = 0.5 \mu s \) and \( t = 0.7 \mu s \), and of the proton density \( n_i \) at \( t \approx 0 \), \( t = 0.5 \mu s \) and \( t = 0.7 \mu s \). The electron current sheet breaks up into the filaments along the \( z = 0 \) plane. The ion density also follows the filamentation.

The distributions of magnetic field strength along \( x = 0 \) are presented in Figures 3 at \( t = 0.0 \), \( t = 0.5 \mu s \), \( t = 0.7 \mu s \) and \( t = 0.8 \mu s \), respectively. At \( z = 0 \) the initial magnetic field changes the sign. The magnetic island formation and the associated magnetic reconnection become remarkable around time \( t = 0.5 \mu s \). The growth rate of the tearing mode instability may be estimated by \( \Gamma_{rec} \approx v_A/L \) [20], which is about \( \Gamma_{rec} \approx 2.18 \times 10^4 /\text{s} \) in our cases. The Alfvén speed \( v_A = v_A \approx 2.18 \times 10^4 /\text{s} \). The modulation scale length \( L \) is approximately equal to 0.01 m. The growth time scale can be estimated as \( \tau \approx 1/\Gamma_{rec} \approx 0.458 \mu s \), which is well consistent with the kinetic simulation results. At \( t = 0.8 \mu s \) the tearing mode instability enters the nonlinear stage. Several magnetic islands have formed in Fig. 3(d).

The corresponding magnetic field vector evolutions are shown in Figures 4 in the plane of \( x = 0 \). Initially, the magnetic vectors are anti-parallel according to \( z = 0 \). With time evolves, the magnetic field lines bend and gradually form the X-point (null-point) with magnetic reconnection, which is clear in Fig. 4(d) at about 1 \( \mu s \). It can be seen that the tearing mode gives rise to the formation of a magnetic island centred in the region of \(-3 < y < 3 \) m. Magnetic field-lines situated outside are displaced by the tearing mode, but still remain their original topology. By contrast, field-lines inside the region have been broken and reconnected with quite different topology.
FIG. 2: (color online) Spatial distribution of the electron number density $n_e$ at (a) $t = 0.5\mu s$ and (b) $t = 0.7\mu s$, and the proton density $n_i$ at (c) $t = 0$, (d) $t = 0.5\mu s$ and (e) $t = 0.7\mu s$. The electron sheet current is filamented along the $z = 0$ plane, and the ions also follow the filamentation.

FIG. 3: (color online) Distribution of magnetic field strength at $x = 0$ at (a) $t = 0.0$, (b) $t = 0.5\mu s$, (c) $t = 0.7\mu s$ and (d) $t = 0.8\mu s$. After $t = 0.5\mu s$ the magnetic reconnection becomes distinct.

In Figs. 5, the slices of current density distribution in the plane of $x = 0$ (the cross section plane), $z = 0$ (the longitudinal plane) and $y = -10\ cm$ (the bottom plane) are shown at (a) $t = 0.5\mu s$ and (b) $t = 1.0\mu s$. The current density $J_x$ is normalized by $n_0e c$. The electron current sheet according to the reconnection X-point is formed in Fig. 5(a) and is significantly amplified in (b). The net current shows the filamentation along with the magnetic reconnection. Now we apply the mechanism of the instability dynamic mitigation to the case of the tearing mode developing in the current sheet. The main purpose of dynamic mitigation mechanism is to saturate the instability growth. It also leads to the smoothing of the modulations in plasmas and fluids, which has been proposed and discussed in detail in Ref. [1–4]. When in an unstable system a physical quantity $\phi$ perturbations depend on time and coordinates in the
FIG. 4: (color online) Distributions of magnetic field vectors along $x = 0$ at (a) $t = 0.2\mu s$, (b) $t = 0.5\mu s$, (c) $t = 0.7\mu s$ and (d) $t = 1.0\mu s$. After $t = 0.5 \mu s$ magnetic reconnection becomes distinct.

FIG. 5: (color online) Distributions of current near the electron current sheet $J_x$ at (a) $t = 0.5\mu s$ and (b) $t = 1.0\mu s$. The net current shows the filamentation along with the magnetic reconnection.

form of
\[
\delta \phi = \delta \phi_0 e^{\Gamma(t-\tau)+ik \cdot x + i\Omega \tau},
\]
the time dependence of modulations $\delta \phi$ is characterized by the growth rate of $\Gamma > 0$. Here $\delta \phi_0$ is the perturbation amplitude, $k$ the wave number vector, $\tau$ the time at which the perturbation is applied, and $\Omega$ defines the perturbation phase. In plasmas, it would be difficult to measure the perturbation phase, and therefore, the feedback control [5] cannot be directly applied to suppress the plasma instability growth. However, the perturbation phase $\Omega \tau$ would be defined externally by, for example, energy-carrying driver oscillation. When the perturbations introduced at $t = \tau$ change the phase continuously by $\Omega \tau$, the overall perturbation superimposed at $t$ is obtained by
\[
\int_0^t d\tau \delta \phi_0 e^{i\Omega \tau} e^{\Gamma(t-\tau)+ik \cdot x} \propto \frac{\Gamma + i\Omega}{\Gamma^2 + \Omega^2} \delta \phi_0 e^{\gamma t} e^{ik \cdot x}.
\]
Although the growth rate $\Gamma$ does not change, the perturbation amplitude is well reduced by the factor of $\sim \Gamma/\Omega$ for $\Gamma \geq \Omega$, compared with that non-phase-oscillation case. The theoretical consideration suggests that the frequency $\Omega$
FIG. 6: (color online) Schematic diagram for dynamic phase control in electron current sheet sustained plasma system, in which electron filamentation and magnetic reconnection grow. The electron sheet current is oscillated along the sheet, and the perturbations induced by the electron beam smooth and mitigate the perturbation amplitude.

in the perturbation phase change should be larger than or at least comparable to $\Gamma$ for the effective mitigation or smoothing of the perturbations.

Here the phase-control dynamic mitigation mechanism is applied to the case of electron current sheet plasma as shown in Fig. 1. The electron beam has a form of thin layer periodic along the $y$ coordinate with the amplitude of 0.1 m, the wavelength in $x$-direction of 0.1 m and with the wobbling frequency $\Omega = 300$ MHz, which is large enough compared with the reconnection growth rate $\gamma_{rec} : \Omega >> \gamma_{rec}$. The corresponding schematic of the dynamic phase control in electron current sheet sustained plasma system is presented in Fig. 6. Since the wobbling electron current sheet is modulated periodically along the current sheet, it is expected that the perturbation phases introduced by the electron beam to smooth and mitigate the instability amplitude compared with the non-wobbling case mentioned above.

Figures 7 show the electron number density $n_e$ and the proton density $n_i$ in the orthogonal slice planes ($x = 0$, $z = 0$ and $y = –10$ cm). The initial distribution of the oscillating or wobbling motion of the electron sheet current is presented in Fig. 7(a). The effects of dynamic mitigation can be clearly seen by comparing the distributions shown in Figs. 7 with Figs. 2. The filamentations (for both electrons and ions) do not grow significantly. Figures 8 show the magnetic field strength at $x = 0$. Due to the suppression of filamentation and the corresponding tearing mode instability, the magnetic field reconnection is also not as remarkable as the non-wobbling case. Comparing with the results presented in Figs. 3, the dynamic mitigation or onset delay of the magnetic reconnection is clearly shown in Figs. 8. There is no X-point or tearing induced separatrix and the magnetic fields are still anti-parallel with respect to the boundary along $z = 0$.

In the electric current distributions $J_x$ at (a) $t = 0.5\mu$s and (b) $t = 1.0\mu$s shown in Fig. 9, although the current density is pinched, the corresponding amplitude becomes much weaker. The current amplitude in the non-wobbling case shown in Fig. 5 ranges from $-0.8 n_0ec$ to $-0.2 n_0ec$. However, experiencing the mitigation, the current amplitude oscillates from $-0.6 n_0ec$ to $-0.4 n_0ec$, which is about 1/3 of the previous amplitude.

In order to compare the filamentation and magnetic reconnection in the electron current sheet sustained plasma system in the case with and without wobbling mitigation, the histories of the normalized field energy of $B_z^2$ are presented in Fig. 10. In our systems in Figs. 1(a) and 6, the major energy is the electron kinetic energy. The perturbations imposed initially lead to the electron current filamentation along with the magnetic reconnection. Associated with the electron current filamentation and the magnetic reconnection, the magnetic field normal component $B_z$ is induced. Figure 10 demonstrates the clear difference in the field energy between the two cases. With the wobbling motion of the electron beam (see Figs. 6 and 7(a)), the onset of the filamentation and of the magnetic reconnection in the current sheet sustained plasma system have been significantly delayed.
FIG. 7: (color online) Electron number density $n_e$ at (a) $t = 0.0$, (b) $t = 0.5\mu s$ and (c) $t = 0.7\mu s$, and the proton density $n_i$ at (d) $t = 0.5\mu s$ and (e) $t = 0.7\mu s$. In Figs. 7 the filamentation does not grow well compared with the results in Figs. 2.

FIG. 8: (color online) Distribution of magnetic field strength along $x = 0$ at (a) $t = 0.3$, (b) $t = 0.5\mu s$, (c) $t = 0.7\mu s$ and (d) $t = 0.8\mu s$. By the electron wobbling motion along $y$, the magnetic reconnection is mitigated well.

DISCUSSIONS AND CONCLUSIONS

The theoretical considerations and 3D numerical computations show the clear effectiveness and viability of the dynamic phase control method to mitigate the plasma instability and the magnetic reconnection. The current sheet plasma system can be found in magnetic fusion devices, space, terrestrial magnetic system, etc. The dynamic mitigation mechanism may contribute to mitigate the magnetic fusion plasma disruptive behavior or to understand the stable structure of the sheet current sustained plasma system. In this paper we focus on the non-relativistic magnetic reconnection and the filamentation (tearing mode like) instability, and the major energy carrier is the sheet electron current. On the other hand relativistic magnetic reconnection has been also studied in space, solar system, planetary magnetic field, etc. In those cases, the main energy is carried by the magnetic field and the electro-
FIG. 9: (color online) Distributions of current near the electron current sheet \( J_e \) at (a) \( t = 0.5 \mu s \) and (b) \( t = 1.0 \mu s \). By the wobbling or oscillating motion of the sheet electron current along \( y \), the onsets of the filamentation and the magnetic reconnection are delayed and mitigated clearly.

FIG. 10: (color online) Histories of the normalized field energy of \( B_z^2 \) for the sheet electron current plasma systems with (solid line) and without (dotted line) the wobbling or oscillating motion of the sheet electron current along \( y \). The onsets of the filamentation and the magnetic reconnection are delayed and mitigated clearly by the dynamic phase control.

magnetic field. In the relativistic magnetic reconnection case, the dynamic mitigation mechanism should be further studied.

METHODS

The simulations are performed with the relativistic electromagnetic code EPOCH \([32]\) in 3D cases. The simulation box has the size of \( L_x \times L_y \times L_z = 20 \text{ cm} \times 20 \text{ cm} \times 20 \text{ cm} \). The mesh size in the simulations is \( \delta x = \delta y = \delta z = 0.1 \text{ cm} \). 64 quasiparticles per cell are employed with a total number of \( 5.12 \times 10^8 \). The real mass ratio of electron and proton \((m_p/m_e = 1836)\) is used in the simulations. Open boundary conditions for fields and reflection boundary conditions for particles are applied in the \( z \)-direction. The periodic boundary conditions are employed for both particles and fields in the \( x \)- and \( y \)-directions. Both the electrons and protons have the initial temperature of 116 keV.

Data availability. The data that support the plots and findings of this paper are available from the corresponding author upon reasonable request.

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AUTHOR CONTRIBUTIONS

Y.J. Gu carried out the simulations, analysed the results, generated the figures. S. Kawata proposed the model, discussed the physics and interpreted the results of the simulations. S. V. Bulanov discussed the physics and did the analytical work. All authors contributed to the preparation of the manuscript.

COMPETING INTERESTS

The authors declare no competing interests.

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[1] Sato, R. et al. Non-uniformity smoothing of direct-driven fuel target implosion by phase control in heavy ion inertial fusion. Sci. Rep. 9, 6650 (2019).
[2] Kawata, S. Dynamic mitigation of instabilities. Phys. Plasmas 19, 024503 (2012).
[3] Kawata, S. et al. Dynamic stabilization of filamentation instability. Phys. Plasmas 25, 011601 (2018).
[4] Kawata, S. et al. Radiation effect on pellet implosion and Rayleigh-Taylor instability in light-ion beam inertial confinement fusion. Laser Part. Beams 11, 757 (1993).
[5] Franklin, G. F., Powell, J., & Emami-Naeini, A. Feedback Control of Dynamic Systems, Global ed. (Pearson Education Ltd., 2014).
[6] Clayton, G. M., Tien, S., Leang, Kam K., Zou, Q., & Devasia, S. A Review of Feedforward Control Approaches in Nanopositioning for High-Speed SPM. J. Dyn. Syst., Meas., Control 131, 061101 (2009).
[7] Bret, A., Firpo, M.-C. & Deutsch, C. Characterization of the Initial Filamentation of a Relativistic Electron Beam Passing through a Plasma. Phys. Rev. Lett. 94, 115002 (2005).
[8] Bret, A., Firpo, M.-C. & Deutsch, C. Collective electromagnetic modes for beam-plasma interaction in the whole k space. Phys. Rev. E 70, 046401 (2004).
[9] Okada, T., & Niu, K. Filamentation and Two-Stream Instabilities of Light Ion Beams in Fusion Target Chambers. J. Phys. Soc. Jpn. 50, 3845 (1981).
[10] Okada, T., & Niu, K. Effect of collisions on the relativistic electromagnetic instability. J. Plasma Phys. 24, 483 (1980).
[11] Hubbard, R. F. & Tidman, D. A. Filamentation Instability of Ion Beams Focused in Pellet-Fusion Reactors. Phys. Rev. Lett. 41, 866 (1978).
[12] Chang, Z., Callen, J. D., Fredrickson, E. D., Budny, R. V., Hegna, C. C., McGuire, K. M., Zarnstorff, M. C. & TFTR group Observation of Nonlinear Neoclassical Pressure-Gradient–Driven Tearing Modes in TFTR. Phys. Rev. Lett. 74, 4663 (1995).
[13] Gu, Y. J. et al. Electromagnetic Burst Generation during Annihilation of Magnetic Field in Relativistic Laser-Plasma Interaction Sci. Rep. 9, 19462 (2019).
[14] Gu, Y. J. et al. Fast magnetic-field annihilation in the relativistic collisionless regime driven by two ultrashort high-intensity laser pulses. Phys. Rev. E 93, 013203 (2016).
[15] Yamada, M., Ren, Y., Ji, H., Breslau, J., Gerhardt, S., Kulskud, R. & Kuritsyn, A. Experimental study of two-fluid effects on magnetic reconnection in a laboratory plasma with variable collisionality. Phys. Plasmas 13, 052119 (2006).
[16] Fujimoto, K. & Sydora, R. D. Plasmoid-Induced Turbulence in Collisionless Magnetic Reconnection. Phys. Rev. Lett. 109, 265004 (2012).
[17] Zenitani, S., Hesse, M., Klimas, A., Black, C. & Kuznetsova, M. The inner structure of collisionless magnetic reconnection: The electron-frame dissipation measure and Hall fields. Phys. Plasmas 18, 122108 (2011).
[18] Zelenyi, L. M., Malova, H. V., Artemyev, A. V., Popov, V. Yu. & Petrakovitch, A. A. Thin current sheets in collisionless plasma: Equilibrium structure, plasma instabilities, and particle acceleration. Plasma Phys. Rep. 37, 118 (2011).
[19] Birn, J. et al. Geospace Environmental Modeling (GEM) magnetic reconnection challenge. J. Geophys. Res. 106, 3715 (2001).
[20] Yamada, M., Kulskud, R. & Ji, H. Magnetic reconnection. Rev. Mod. Phys. 82, 603 (2010).
[21] Priest, E. & Forbes, T. Magnetic Reconnection. MHD Theory and Applications. (Cambridge University Press, 2000).
[22] Zelenyi, L. M., Malova, H. V., Artemyev, A. V., Popov, V. Yu. & Petrakovitch, A. A. Thin current sheets in collisionless plasma: Equilibrium structure, plasma instabilities, and particle acceleration. Plasma Phys. Rep. 37, 118 (2011).
[23] Birn, J., Artemyev, A. V., Baker, D. N., Echim, M., Hoshino, M. & Zelenyi, L. M. Particle Acceleration in the Magnetotail and Aurora. Space Sci. Rev. 173, 49 (2012).
[26] Wesson, J. Tokamaks (Oxford Science Publications, Oxford, 2003).
[27] Pegoraro, F. & Veltri, P. The unusual properties of plasmas. La Rivista del Nuovo Cimento 43, 229 (2020).
[28] Remington, B. A., Drake, R. P. & Ryutov D. D. Experimental astrophysics with high power lasers and Z pinches Rev. Mod. Phys. 78, 755 (2006).
[29] Bulanov, S. V., Esirkepov, T. Zh., Habs, D., Pegoraro, F. & Tajima, T. Relativistic laser-matter interaction and relativistic laboratory astrophysics. Eur. Phys. J. D 55, 483 (2009).
[30] Bulanov, S. V. Magnetic reconnection: from MHD to QED. Plasma Phys. Controlled Fusion, 59, 014029 (2017).
[31] Harris, E. G. On a plasma sheath separating regions of oppositely directed magnetic field. Nuovo Cimento 23, 115 (1962).
[32] Arber, T. D. et al. Contemporary particle-in-cell approach to laser- plasma modelling. Plasma Phys. Control. Fusion 57, 113001 (2015).
[33] Kuramitsu, Y. et al. Magnetic reconnection driven by electron dynamics Nat. Commun. 9, 5109 (2018).
[34] Gu, Y. J. & Bulanov, S. V. Magnetic field annihilation and charged particle acceleration in ultra-relativistic laser plasmas. High Power Laser Sci. Eng. 9, e2(2021).