Soft gamma-ray background and light Dark Matter annihilation

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The bulk of the extragalactic background between 10 keV and 10 GeV is likely to be explained by the emission of Seyfert galaxies, type Ia supernovae, and blazars. However, as revealed by the INTEGRAL satellite, the bulge of our galaxy is an intense source of a 511 keV gamma-ray line, indicating the production of a large number of positrons that annihilate. The origin of the latter is debated, and they could be produced, in particular, by the (S- or P-wave) annihilation of light Dark Matter particles into $e^+e^-$. In any case, the cumulated effect of similar sources at all redshifts could lead to a new background of hard X-ray and soft gamma-ray photons. On the basis of the hierarchical model of galaxy formation, we compute analytically the SNIa contribution to the background, and add it to Seyfert and blazars emission models. Confronting these expected contributions to observation, we find that any extra contribution to this unresolved background around 511 keV should be lower than about 4 keV cm$^{-2}$ s$^{-1}$ sr$^{-1}$. We also estimate analytically the extragalactic background due to Dark Matter annihilation, increasing the accuracy of the earlier computations. Indeed, we take into account the large positron escape fraction from low mass dark matter halos, unable to confine a dense and magnetized interstellar medium. Our new background estimate turns out to be one order of magnitude lower so that the hypothesis of a light Dark Matter candidate remains compatible with the observed extragalactic background for a wider range of particle masses and cross-sections.

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I. INTRODUCTION

The cosmic gamma-ray background (CGB) between 10 keV and 10 GeV has been measured by several gamma-ray satellites (HEAO, SMM, COMPTEL and EGRET) [1, 2]. Below 100 keV, it is believed that the main contribution comes from Seyfert galaxies [1, 3]. Above 10 MeV, a simple model for blazars reproduces both the amplitude and the slope of the data [4]. In the intermediate energy range, however, another type of sources is needed, since blazar spectra show a clear break near 10 MeV and the cosmological gamma-ray background from Seyfert galaxies falls off above about 100 keV (see Fig. 1). As discussed by several authors [5, 6, 7], type Ia supernovae could make a significant contribution in this energy range, which we shall evaluate in Section 2.

Furthermore, the recent observation, by the INTEGRAL satellite, of a 511 keV diffuse emission line from the galactic bulge [8] shows that electron-positron annihilation are taking place there with a very large rate $\simeq 1.5 \times 10^{43}$ s$^{-1}$. Such a high rate is difficult, if not impossible, to impute to astrophysical objects, and the source of these positrons in the bulge is subject to intense debate. This emission from the bulge of the Milky Way could be the signature of light Dark Matter particles annihilating into $e^+e^-$. In any case, the cumulated effect of similar sources at all redshifts could lead to a new background of hard X-ray and soft gamma-ray photons.

Since the potential implications of such an hypothesis for particle physics and cosmology are very important, we want to test here its validity or at least its consistency, as far as the cosmological gamma-ray background is concerned. Using a recent model of galaxy formation [12], we compute self-consistently the gamma-ray background coming from both type-Ia supernovae (adding Seyfert-galaxies and blazars), and annihilating positrons from light Dark Matter halos. We follow in this respect the earlier work of Ahn & Komatsu [13], who were the first to compute this background, assuming, like them, how-

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ever, that positrons annihilate “on the spot” in all Dark Matter halos in the Universe. These authors explored various scenarios for the internal structure of Dark Matter halos and analyzed how these various models affect the amplitude of the gamma-ray background.

In the present paper, we would like to go one step further, and explicitly take into account the role of baryons in the process of positron confinement and annihilation. This process is indeed possible only if the parent halo contains enough baryons (and therefore also electrons) to host a dense, magnetized, interstellar medium. This is a necessary condition for the “on the spot” approximation to be valid. Since low mass halos are unable to host enough baryons in a cold and magnetized disc [12], the escaping positron mean free path increases dramatically. To compute the positron escape fraction and their propagation in the expanding background, a complex diffusion study would be necessary. As a first order approximation we shall assume that the positron escape fraction goes from zero to one below the critical mass for a Dark Matter halo to host a galaxy, as computed in [12], and that these escaping positrons never annihilate.

The outline of this article is as follows. In Section 2, we estimate the contribution of SNIa to the gamma-ray background, adding it to that of Seyfert galaxies and blazars (at lower and higher energies, respectively). The difference with the observed spectrum provides an upper limit on any additional contribution such as the one due to annihilating positrons, that could come from light Dark Matter particle annihilation. In Section 3, we calculate the diffuse cosmological background induced by all Dark Matter halos in the Universe, taking into account that positrons cannot annihilate in small mass halos, and compare it to the previous calculation performed by Ahn & Komatsu [13]. In Section 4, we present the gamma-ray background constraints on the annihilation cross-sections and the masses of light Dark Matter candidates. We summarize our main conclusions in Section 5. In an Appendix, we estimate for calibration purpose, and confront with SPI/INTEGRAL observations, the 511 keV emission from the galactic bulge. We consider various annihilation cross-sections (depending on whether they are S- or P- wave dominated) and the corresponding halo Dark Matter density profiles.

II. DIFFUSE GAMMA-RAY BACKGROUND FROM SNIA

The type Ia supernovae contribution to the gamma-ray background depends primarily on the star formation history in the Universe, which, in this paper, is derived from a new self-consistent model of galaxy formation [12]. This analytical model predicts the cosmological evolution of the four main baryon phases in the Universe: diffuse intergalactic gas, hot gas, cold gas in galaxies and stars. These theoretical predictions were validated with high-resolution cosmological simulations using the RAMSES [14] and GADGET codes [15]. They also reproduce the observed amount of cold gas in the Damped Lyman-Alpha systems [16, 17] and the observed Cosmic Star Formation Rate [18, 19, 21, 22, 23, 24, 25] (see Fig. 2), which is of prime interest here. The model particularly emphasizes the important cosmological role of the minimal mass for a halo to host galaxies, $M_{\text{min}}(z)$.

We shall use it to, first, compute the SNIa gamma-ray background, and, also, to evaluate the new background that could be attributed to the annihilation of positrons, possibly generated in annihilating Dark Matter halos. This internal consistency allows us to perform a fair comparison between the two types of gamma-ray sources.

In the general case, the background intensity $I_{\nu}$ is given by

$$I_{\nu} = \frac{c}{4 \pi} \int_{0}^{t_{\nu}} j_{\nu}(\nu(1+z), z) \, dt,$$  \hspace{1cm} (1)

with $j_{\nu}(\nu, z)$ the comoving emissivity at redshift $z$, or time $t$.

The gamma-ray lines from SNIa result from the explosive synthesis of radioactive $^{56}\text{Ni}$ nuclei, decaying succes-
served extragalactic background below 100 keV and physical sources reproduces reasonably well the observed rates suggested by recent observations [12].

Our star formation history is slightly more efficient, as slightly higher than their preferred model [49], because with the SNIa contribution from Strigari et al. [6], is galaxies and blazars. This contribution, in agreement to be close to the predicted contributions from Seyfert

The resulting extragalactic background spectrum from known as-

\[ \rho_X(r) \propto \frac{1}{x^\gamma(1 + x^\alpha)^{-1}}, \]

above 3 MeV. However, in the range from 100 keV to 3 MeV the three contributions fall short of explaining the bulk of the Cosmic Gamma-Ray background (as emphasized by Strigari et al. [6]). Particularly, in the 100 keV-511 keV range of interest in this article, the sum of the three contributions appears to be lower with a difference of the order of 4 keV cm\(^{-2}\) s\(^{-1}\) sr\(^{-1}\). This sets an upper limit on a possible Dark Matter annihilation signal.

III. DIFFUSE BACKGROUND FROM COSMOLOGICAL HALOS

A. Diffuse background

The diffuse background is simply the sum of the redshifted emissions from positron annihilation in all cosmological halos, in principle at all redshifts (Eq. 1). The comoving emissivity can be computed by summing up the individual halo emissivities

\[ j_\nu(v, z) = \int_{0}^{\infty} \frac{dN}{d\ln M d\nu} \frac{L_\nu(M, z)}{M} d\ln M \]  (3)

where \( M_{\text{min}} \) is the minimal mass for emitting halos. The luminosity per halo integrated up to the radius of the halo \( R_{200} \) is

\[ L_\nu(M, z) = \int_{0}^{R_{200}} P_\nu(r) 4\pi r^2 dr, \]  (4)

and \( N(M, z) \) is the Press-Schechter [27] mass function for cosmological halos. Considering positron annihilation “on the spot”, the volume emissivity is given by

\[ P_\nu(r) = \frac{1}{2} S_{\text{pos}}(\nu) \rho_X^2(r) \frac{\langle \sigma v_{\text{rel}}(r) \rangle}{m_X^2}, \]  (5)

with \( \rho_X(r) \) the Dark Matter mass density profile, \( \langle \sigma v_{\text{rel}}(r) \rangle \) is the annihilation cross-section, the factor \( \frac{1}{2} \) being present only in the case of self-conjugate Dark Matter particles [54].

Positronium annihilation introduces a specific emission spectrum \( S_{\text{pos}}(\nu) \), with 25% of the energy injected in the 511 keV line, and the remaining 75% spread over a 3\(\gamma\) continuum.

B. Dark matter density profile

The mass distribution in each Dark Matter halo is in fact quite uncertain. Ahn and Komatsu [12] have explored a wide range of halo density profile parameters. In this paper, we restrict ourselves to Dark Matter distribution parameters at face value, as suggested by N-body simulations, based on the following general fitting formula

\[ \rho_X(r) \propto \frac{1}{x^\gamma(1 + x^\alpha)^{-1}}, \]  (6)
where $x = r/r_s$ with $r_s$ the scaling radius corresponding to the concentration parameter $c = R_{200}/r_s$ (typically between 4 and 40 depending on halo mass and redshift). $\gamma$, $\alpha$, and $\beta$ control the slope respectively for small ($r < r_s$), intermediate ($r \approx r_s$) and large radii ($r > r_s$).

The concentration parameter defines whether halos are rather peaked ($c \approx 40$) or shallow ($c \approx 4$). Here again the mean value as a function of redshift and halo mass is given by a fit on cosmological simulations [23],

$$c = \max(4, 4 \left( \frac{1 + z_c}{1 + z} \right))$$

with $z_c$ the collapse redshift given by $M_s(z_c) = 10^{-2} M$, $M_s$ being the non-linear mass at a redshift $z$. This formula is valid only for halos greater than $\approx 10^{3} M_\odot$. The behaviour of the concentration parameter for smaller halo masses, unresolved by numerical simulation, is totally unknown.

The slope at the center of Dark Matter halos is thought to be between $\alpha = 1$ and $\alpha = 1.5$. We therefore consider two extreme dark matter profiles as given by Navarro, Frenk and White [20] ($\alpha = 1, \beta = 3$ and $\gamma = 1$) and Moore [30] ($\alpha = 1.5, \beta = 3$ and $\gamma = 1.5$). Note however that both density profiles saturate at very low radius $R_{\min}$ when $n(R_{\min}) = \sigma v_{\text{rel}}(r) = 1/t_H$ due to self-annihilation ($n(R_{\min}) = \rho_X(R_{\min})/m_X$ is the dark matter numeric density and $t_H$ is the age of the universe).

### C. Annihilation cross-section

The relic abundance of Dark Matter particles depends on their decoupling temperature, which is a fraction of their mass (i.e. $T_F = \frac{m_X}{x_F}$ with $x_F \approx 16$ to 20 depending on $m_X$) and is, roughly, inversely proportional to their annihilation cross-section $\langle \sigma v_{\text{rel}} \rangle_F$ at freeze-out. The values required for a correct abundance, corresponding to $\Omega_{\text{DM}} \approx 23\%$, are then, for such light particles, of the order of a few (up to $\approx 10$) picobarns (corresponding to $\langle \sigma v_{\text{rel}} \rangle F \approx 10^{-25}$ cm$^3$ s$^{-1}$) [3, 10], depending on whether they are self-conjugate or not, and on the possible velocity-dependence of their annihilation cross-section at freeze-out.

Such values are in any case rather large compared to ordinary weak-interaction cross-sections, especially when dealing with light particles. This necessitates an unusual, more powerful, annihilation mechanism, that could result from the exchanges of a new light neutral gauge boson $U$, or, in the case of spin-0 Dark Matter particles, from the exchanges of new heavy (e.g. mirror) fermions [3, 10].

A rather large annihilation cross-section could lead to an excessive continuum of gamma-ray photons at various energies (depending on $m_X$). Cross-sections which behave, at least to a large extent, proportionally to $v^2$ ($P$-wave annihilation), may therefore be preferred [32], especially at lower $m_X$. The residual annihilation of Dark Matter particles in bulges of spiral galaxies or in ellipticals would then include a suppression factor that could be, in the pure $P$-wave case, as strong as $v_{\text{halo}}^2/v_{\text{c}}^2 \approx 10^{-5}$. Furthermore, and independently of the above argument, lighter Dark Matter masses $m_X$ tend to be preferred, to avoid excessive gamma-ray production as compared to $e^+$ production, in our galaxy [10, 32].

We shall therefore consider annihilation cross-sections parametrized as $\sigma v_{\text{rel}} \approx a + b v^2$, with $\langle \sigma v_{\text{rel}} \rangle_F \approx 10^{-25}$ cm$^3$ s$^{-1}$ at freeze-out (for a self-conjugate particle – or twice this value, for a non self-conjugate one). And explore in particular, for low-velocity halo particles, the two extreme situations $\langle \sigma v_{\text{rel}} \rangle \approx a$ ($S$-wave) and $\approx b v^2$ ($P$-wave annihilation). The resulting emission profiles deduced from a given Dark Matter profile $\rho_X$ are computed from $\langle \sigma v_{\text{rel}} \rangle \rho_X^2/m_X^2$ (cf. Eq. 6 for a self-conjugate particle). See also the Appendix for further comments.

Note that for the pure $P$-wave cross-section, the emissivity now depends on the Dark Matter 3D velocity dispersion. We therefore compute $\sigma_{2D}^2$ as a function of the radius by solving the Jeans equation for a NFW or Moore potential. The resulting emission profiles turn out to be less peaked than for a pure $S$-wave cross-section.

### D. Role of the baryons

This rather standard approach has been applied to compute the soft gamma-ray background in [12], integrating individual halo emissivity over the Press & Schechter distribution (given by Eq. 6), using as lower bound of the integration interval the maximum between

![FIG. 3: Redshift evolution of the minimal halo mass $M_{\text{min}}$ below which cold disk gas cannot form (see 12 for details). We use a reionization redshift $z_r \approx 20$ as suggested by WMAP.](image-url)
the Dark Matter free-streaming and the Dark Matter Jeans masses. This leads to a minimal mass ($M_{\text{min}}$) equal to a fraction of solar mass. As a consequence the comoving gamma-ray emissivity is dominated by the cumulated emission of numerous small mass halos (if one uses the concentration parameters given by Eq. [52]).

However, as we have already discussed, small mass halos are unable to retain gas and annihilate positrons, and therefore cannot contribute to the gamma-ray background in which we are interested. We take into account the crucial role of the baryons (and associated electrons, and magnetic fields) in confining and annihilating the Dark Matter positrons. This trapping can be achieved only if both the density of the interstellar medium and the galactic magnetic field are sufficient. Indeed cosmological simulations of structure formation in the hierarchical framework of structure formation show that baryons cannot collapse and form high-density centrifugally-supported gas discs in halos having a mass lower than a minimal value $M_{\text{min}} \approx 10^7 - 10^{11} h^{-1} M_\odot$.

This critical mass threshold is a key ingredient of the current galaxy formation theory. Gnedin showed that the fraction of baryons decreases strongly in halos smaller than the so-called filtering mass $M_{\text{filter}}$, as a consequence of the non-zero temperature of the intergalactic medium which prevents gas from collapsing into too small Dark Matter halos. Hoeft et al. [36] also showed that the halo mass must be greater than the minimal cooling mass; if not, the fraction of baryons is high but galaxies cannot form because cooling is inefficient. The resulting minimal halo mass $M_{\text{min}}$ for galaxy formation is then the maximum between the minimal cooling mass and the filtering mass, as computed in [32]. The evolution of this minimal mass with redshift is shown in Fig. 5. It is of course much larger than the one used in [13].

As computing accurately the escape fraction of positrons as a function of halo mass is beyond the scope of this paper, we shall consider here, for simplicity, that below $M_{\text{min}}$, essentially all positrons escape the halos (and we neglect their contribution to the background), while above $M_{\text{min}}$, confinement is supposed to be efficient and all positrons are taken to contribute. Furthermore, the contribution from diffuse baryons in the Universe (baryons which are not in collapsed halos) is negligible in this range of wavelength because the annihilation time scale is larger than the age of the Universe [52]. Note that, while the “on the spot” approximation, used by Ahn & Komatsu [13] for the whole mass range, leads, in our opinion, to an overestimation of the diffuse background, our approach, though more accurate, should lead to an underestimation of the background level.

Fig. 4 illustrates the distribution of comoving positron emissivity as a function of halo masses for different redshifts. The comoving emissivity is dominated by small mass halos. However, only a small fraction of the halos contains enough gas and magnetic field for the production of gamma-rays: altogether, only a fraction of about 10% of the emitted positrons are converted into photons.

As a consequence, our computation of the gamma-ray background leads to a result about 10 times smaller than the one evaluated by Ahn and Komatsu [13].

More precisely, we have computed the soft gamma-ray background for direct annihilation with a $S$-wave cross-section, a NFW Dark Matter density profile and a particle mass $m_X = 20$ MeV in the two different cases: dark matter-based minimal mass as in [13] and baryon-based minimal mass as in the present paper. Fig. 5 illustrates the decrease by a factor of 10 using our new approach. Thus, if we would like to reach the same level of background, we would have to divide the particle mass $m_X$ by a factor of $\sqrt{10}$.

Note that the spectral shape is also modified. The spectrum declines at low energy because it corresponds to high redshift where halos greater than the minimal mass for galaxy formation becomes rare. Note that in Ahn and Komatsu [13], identical results were recovered for the same Dark Matter particle mass, using rather extreme values for the halo concentration parameter $c$. Recall that here we consider halo concentration parameters only at face value, as predicted by N-body simulations, but we take into account baryon physics as part of the annihilation mechanism.
As we have seen in the previous sections, the diffuse gamma-ray background depends on three main quantities. The first is the annihilation cross-section: we are going to explore two extreme cases: $S$-wave and $P$-wave. The second ingredient is the dark matter mass density profile: we are going to test peaked distributions (Moore, $c=15$) and shallow ones (NFW, $c=5$). The last unknown quantity is the dark matter particle mass $m_X$. In this Section, we are going to fix the latter (for a given set of annihilation cross-section and density profile) using the constraint set by the detected galactic signal.

The line emission at 511 keV detected by INTEGRAL from the galactic center region is at a level of $10^{-3}$ ph cm$^{-2}$ s$^{-1}$ [8]. Several types of astrophysical sources have been considered as potential candidates to explain this emission. However, SNeIa fall short sustaining the high positron injection rate [37, 38]. Hypernovae [39] and the related gamma-ray bursts [37, 39, 40, 41] are in a better position, but since the number of massive stars is about ten times larger in the disk than in the bulge, hot spots of 511 keV emission should show up in the disk plane [54], which is not the case. Low mass X-ray binaries have also been suggested [38], but no 511 keV emission has been observed from these objects. We therefore consider the hypothesis that light Dark Matter particles annihilate into electron-positron pairs, mainly in the galactic center region where the Dark Matter density is at a maximum [9, 10, 11, 12]. The resulting low-energy positrons are confined by the magnetic field of the bulge, where they are progressively slowed down by ionisation losses. A large fraction (0.93) forms positronium with ambient electrons and annihilate into two (25% of probability) or three $\gamma$ photons [42]. Positronium formation plays therefore an important role because it decreases by a factor of about 3 the intensity of the 511 keV line.

The flux of gamma rays (from a direction making an angle $\theta$ with the direction of the galactic center) is given by the integral of the emissivity along the line of sight

$$F_\nu(\theta) = \frac{1}{4\pi} \int_{\text{los}} P_\nu(r) \, dl ,$$  \hspace{1cm} (8)

where $P_\nu(r)$ is the volume emissivity. We assume that essentially no annihilation can take place outside the stellar bulge, due to a lack of gas (corresponding roughly to an angle $\theta_{\text{bulge}} = 16^\circ$).

The resulting profiles are convolved with the INTEGRAL/ SPI Point Spread Function (PSF). This method allows a fair comparison between observations and models, and depends only weakly of the poorly known size of the gaseous bulge. For each couple of cross-section - dark matter profile, we have computed which mass $m_X$ fits best the observed level of 511 keV emission. The results are summarized in Table I.

\begin{table}[h]
\begin{center}
\begin{tabular}{|c|c|c|}
\hline
$m_X$ (MeV) & $S$-Wave & $P$-Wave \\
\hline
Moore $c=15$ & 1500 & 2.4 \\
Moore $c=10$ & 900 & 1.2 \\
Moore $c=5$ & 440 & 0.44 \\
NFW $c=15$ & 190 & 0.42 \\
NFW $c=10$ & 110 & 0.20 \\
NFW $c=5$ & 45 & 0.060 \\
\hline
\end{tabular}
\end{center}
\caption{This Table summarizes, for different cases, which dark matter particle mass (in MeV) is (or would be) required to reproduce the level of the INTEGRAL signal from the galactic bulge. We explore different cross-sections ($S$-wave or $P$-wave), different inner slopes (Moore or NFW) and different concentration parameters ($c=5 - 15$). (A result smaller than $\frac{1}{2}$ MeV indicates that the signal cannot be reproduced with the annihilation cross-section and density profile considered.)}
\end{table}
\(m_X < 0.42 \text{ MeV}\) so small that they are unable to produce 511 keV photons. And the Moore \(S\)-wave case required such high masses \(m_X > 440\ \text{MeV}\) that they would lead to an excessive bremsstrahlung emission of soft gamma-ray photons.\footnote{33,}\footnote{33.}

Among the specific cases considered two models (NFW with \(S\)-wave and Moore with \(P\)-wave) are therefore favored by the galactic signal. If one considers only the total emission from the bulge, neither the \(S\)-wave nor the \(P\)-wave cross-section can be excluded. If one considers the emission profile however, a different conclusion could be drawn: according to a recent article \footnote{34.}\footnote{34.}, the shape of the emission profile could be used to exclude the \(P\)-wave scenario. We address this interesting question in the Appendix, in which we conclude that, to our opinion, both scenarios cannot be discriminated yet.

F. Results

As shown in Fig. 6 the background predictions in the two models are at the same level with a slightly different spectral signature. The main conclusion is that the level of the predicted background is more than a factor of 100 below the observed background. Calibrating on the Milky Way, the relative smallness of the obtained results for the cosmic gamma-ray background shows that the light Dark Matter annihilation hypothesis is by far not ruled-out by the current soft gamma-ray extragalactic background constraint.

Note that this conclusion can be applied more generally to other positron sources since the 511 keV emission from the Milky Way is quite weak compared to the observed background intensity. In order to make this background large, one has to assume that other galaxies have much higher positron production rates than the Milky Way. Indeed, in this case, the Milky Way would not be representative from other halos of the same mass.

IV. CONSTRAINTS ON DARK MATTER CANDIDATES

The main objective of this paper is the computation of the Dark Matter induced background in the 100 keV-511 keV energy range taking into account the important role of baryons. Using standard concentration parameters for the Dark Matter halo profiles (as given by N body simulations), the net result of this exercise is a decrease by a factor of 10 of the level of the background emission compared to the precedent computation in \footnote{13.}\footnote{13.}.

Calibration of \(\langle \sigma v \rangle\) \footnote{13.} and \(m_X^2\) on the INTEGRAL signal is however uncertain. Indeed, it depends strongly on the Milky-Way Dark Matter profile which is not well known. The grey region in Fig. 7 shows the range of allowed parameters corresponding to this calibration. To obtain this domain we have considered a reasonable range of Dark Matter profiles from peaked and concentrated ones (Moore profile and \(c = 15\)) to less peaked and less concentrated ones (NFW and \(c = 5\)). Then we have found for each profile which cross-section and particle mass reproduce the level of the galactic emission. As a result, each mass and cross-section in the grey region could reproduce the level of the bulge emission with a reasonable Dark Matter profile. The corresponding background is below the observed background (see the previous Section). As a consequence, no light Dark Matter candidate is ruled out by the diffuse background constraint and one has to invoke another gamma-ray source in order to explain the missing 4 keV cm\(^{-2}\) s\(^{-1}\) sr\(^{-1}\).

If we consider now that the Milky-Way Dark Matter halo is totally different from other halos of similar mass in the Universe, we could relax the previous calibration and obtain independent constraints on the mass and the cross-section (following in that sense the strategy used in \footnote{13.} on the observed background only). In the present paper, constraints are of course less stringent than in \footnote{13.}, since baryon physics has led us to decrease the level of the

![FIG. 6: Diffuse background spectrum. Crosses: HEAO data; stars: COMPTEL observations. The continuous line is the sum of the contributions from Seyferts, SNIIa and blazars. The dot-dot-dot-dashed line and the dashed line represent the revised positron contribution to the cosmological gamma-ray background, for a \(S\)-wave cross-section with a NFW profile, and a \(P\)-wave cross-section associated to a Moore profile, respectively.](image)
FIG. 7: Constraints on the dark matter candidate in the \( a - m_X \) plane, with \( a \) the velocity-independent part in the annihilation cross-section \( \sigma v_{\text{rel}} \) and \( m_X \) the mass of the dark matter particle. \( b \) is fixed by the relic density requirement, so that \( \langle \sigma v_{\text{rel}} \rangle_F \approx a + b v^2 \approx 10^{-25} \text{ cm}^3 \text{ s}^{-1} \) at freeze-out. The upper line \( a \approx 10^{-25} \text{ cm}^3 \text{ s}^{-1} \) corresponds to a purely \( S \)-wave cross-section, and the lower part of the diagram to a \( P \)-wave dominated one (\( a \) being negligible). As \( m_X \) cannot be too large, in order not to overproduce gamma and radio continuum from the galactic center, we limit ourselves, conservatively, to the interval 0.511 to 100 MeV (the actually-allowed mass interval could in fact be significantly smaller depending on how seriously these other constraints are taken).

The grey region is the one compatible with the galactic constraint, based on the total level of emission, using the (Moore or NFW) dark-matter distributions of Table I (its upper part corresponds to a Milky-Way emission that would-be \( S \)-wave-dominated, with \( a \) behaving like \( 1/m_X^2 \)). The dot-dashed line is associated with a dark-matter induced background (for a NFW profile) that would correspond to the missing 4 keV cm\(^{-2}\) s\(^{-1}\) sr\(^{-1}\), the top left-hand corner above this line being excluded on the basis of the cosmic background data (same for the dashed line with Moore profiles).

As shown in Fig. 7, constraints exclude only the upper left hand corner, corresponding to low-mass Dark Matter particles and \( S \)-wave dominated cross-section. Interestingly, for halos with a Moore profile, the Dark Matter candidate mass and cross-section required to reach the level of the observed background are not so far from the region favored by the galactic constraints.

V. CONCLUSIONS

Having estimated the SNIa contribution in the 100 keV-10 MeV energy range, we have found that an unexplained gamma-ray background emission at most of the order of 4 keV cm\(^{-2}\) s\(^{-1}\) sr\(^{-1}\) remains. As proposed in [11], the strong 511 keV emission from the galactic center detected by the INTEGRAL satellite could be explained by light Dark Matter annihilation, and we have verified that the observed emission profile can be reproduced, both for \( S \) and \( P \)-wave annihilation cross-sections. Using the hierarchical model of structure formation, we have computed the corresponding gamma-ray background, and found it to be compatible with current observational bounds, if one takes into account the minimal halo mass for galaxy formation. The new positron-generated (Dark Matter-induced) extragalactic background is in fact overwhelmed by other emissions from SNIa, Seyferts, and blazars. The exclusion of small mass halos as (redshifted) 511 keV photon sources leads to an order of magnitude decrease of the extragalactic flux around 500 keV as compared to earlier studies. The spectral shape of the extragalactic background is also modified in the sense that the number of Dark Matter halos capable of hosting gas rich galaxies decrease very strongly with increasing redshift.

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APPENDIX A: 511 KEV EMISSION FROM THE GALACTIC BULGE

The computation of the Milky-Way emission profile $F(\theta)$ is not the main goal of this paper, since we only used the integrated emission (and not the shape) for calibration purposes. However, it is essential to compare carefully predicted profiles to the observed one (see the recent paper [34]). In this Appendix, we would like to outline some interesting issues concerning this point. Using the same hypothesis as in Section 2, we consider the three different cases of Table I: a NFW profile with a non self-conjugate $S$-$\nu$-wave cross-section; a NFW profile with a Moore profile with a non self-conjugate $S$-$\nu$-wave cross-section; and finally, a Moore profile with a Moore profile with a NFW profile with a non self-conjugate $S$-$\nu$-wave cross-section. In the pure $S$-$\nu$-wave case with an essentially constant density, the annihilation cross-section gets doubled, so that the expected emissivity and resulting emission profile remain the same.

Moreover the concentration parameters of these small halos are quite uncertain because they are smaller than the numerical resolution of cosmological simulations.

Indeed, direct annihilation of positrons having escaped out of small halos as well as annihilation through positronium in the intergalactic medium are negligible (for $z < 50$) due to the very low density of the latter (about $2 \times 10^{-7} (1 + z) ^3 \text{cm}^{-3}$).

Except if positrons escape rapidly from the thin disk, where the gas is concentrated.

\[ P_\nu(r) = S_{\nu\bar{\nu}}(\nu) \rho_X(r) \rho_{\bar{X}}(r) \frac{\langle \sigma v_{\text{rel}} \rangle}{m_X}, \]

and one can generally assume equal densities for Dark Matter particles and antiparticles, so that $\rho_X(r) = \rho_{\bar{X}}(r) = \frac{1}{2} \rho_{\text{tot}}(X + \bar{X})(r)$. For non self-conjugate particles, the $\frac{1}{2} \rho_{\text{tot}}^2$ gets replaced by $\rho_X \rho_{\bar{X}}$ or simply $\frac{1}{2} \rho_{\text{tot}}^2$ while the annihilation cross-section gets doubled, so that the expected emissivity and resulting emission profile remain the same.

\[ \langle \sigma v_{\text{rel}} \rangle \approx a \approx 10^{-22} \text{ cm}^2 \text{ s}^{-1}, \]

we have chosen to consider and test, with the above NFW distribution, a Dark
Figure 8: INTEGRAL/SPI overall counting rate in the 511 keV line as a function of the angular distance to the galactic center. Points with error bars show the instrumental background subtracted count rate of the SPI camera in the 506 to 516 keV band, averaged over the first year of data.

Lines indicate the expected counting rates for three different situations: $S$-wave annihilation cross-section with a NFW Dark Matter profile (continuous line); or $P$-wave cross-section with a NFW (dashed line) or Moore (dotted line) profile, as specified in the text. The figure does not show the actual 511 keV emission profiles, but the results of their convolution with the spectrometer’s response, the Point Spread Function (PSF) — which is a crude but more rigorous way in order to compare data with models. The lower dot-dashed line shows the rate (not compatible with the data) that would correspond to a pointlike source. For the calibration, we choose the Dark Matter particle mass so that the observed integral of the signal over the inner 16 degrees is equal to the one from the theoretical profile.

Matter particle with mass $m_X = 110 \text{ MeV}/c^2$. Let us note however that, given our hypothesis, the same emission profile would have been obtained from the same $\rho_X$ but with a mass of $\approx 11$ (or 1.1) MeV/$c^2$ only, and an $a$ term that would be $\approx 100$ (or $10^4$) times smaller. The corresponding ($S+P$-wave) cross-section would then be $P$-wave dominated at freeze-out, while appearing as $S$-wave-dominated for low-velocity annihilation in the galactic center.

In the pure $P$-wave case on the other hand, for which the annihilation cross-section in the galactic center $\langle \sigma v_{\text{rel}} \rangle$ should be lower (i.e. typically $\approx 10^{-30} \text{ cm}^3 \text{ s}^{-1}$), $m_X$ should in general be taken relatively small, to get (with a correct relic density) a sufficiently intense gamma-ray line. In practice we test $m_X$ about 0.5 (with the NFW profile) and 1.2 MeV/$c^2$ (with the Moore profile).

At first sight, all three tested profiles seem compatible with the observations, within the precision of the analysis. Attempting to discriminate between them (or with analogous ones) would require a careful chi-squared analysis and is beyond the scope of this article, as we are mainly interested here in the total observed intensity and global morphology of the 511 keV emission of the galactic bulge.

If the cross-section for Dark Matter annihilation in halos is velocity-independent ($S$-wave or effectively $S$-wave annihilation), the emissivity of a NFW Dark Matter halo scales near the center as $P_{\nu} \propto r^{-2}$. Convoluting this emission with the SPI Point Spread Function (PSF), we obtain the profile presented as a continuous line in Fig. 8. We emphasize here that the profiles shown are the profiles after convolution by the PSF.

If, however, this cross-section is $S$-wave suppressed, the emissivity now depends on the Dark Matter 3D velocity dispersion. We then compute $\sigma_{\text{rel}}$ as a function of the radius by solving the Jeans equation, at first for a NFW potential. The resulting emission profile (shown after convolution as a dashed line in Fig. 8) also turns out to fit the data, although it is less peaked, as the velocities increase with $r$, within the region of interest. Furthermore, as mentioned earlier, to get in this case the appropriate intensity for the 511 keV line we need to consider both rather small values of $m_X$ (about 0.5 MeV/$c^2$) and somewhat extreme parameters for the Milky-Way Dark Matter halo (choosing $c \approx 15$).

These restrictions may be avoided to some extent, however, with a steeper profile such as the Moore profile, which enhances the rate of Dark Matter annihilation, especially near the center of the galaxy, so that the resulting emission profile (shown after convolution as a dotted line in Fig. 8) gets now more peaked. With such profiles, $P$-wave annihilation with standard Milky-Way parameters appear to be compatible with the data, even for less small values of $m_X$. Furthermore, note that if Dark Matter is subject to the stellar gravitational potential that dominates the central region of the galaxy, with a radial density profile declining roughly as $r^{-2}$. The $S$- and $P$-wave cases would be essentially indistinguishable.

To conclude this Appendix, we have verified that one can reproduce the photon flux and distribution observed by INTEGRAL, both for $S$- and $P$ wave cross-sections, with standard Dark Matter profiles $\rho_X$ and appropriate mass $m_X$. Again, in this approach, attempting to further discriminate between emission profiles associated with $S$- or $P$-wave annihilation appears as difficult, given the width of the PSF function and the variety of the Dark Matter profiles, gravitational potential profiles and gas density profiles which may be considered.