Depth persistence of the spatial pattern of soil–water storage along a small transect in the Loess Plateau of China

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1. Introduction

Soil–water content is a key variable in many hydrological and biological processes (Entin et al., 2000; Western et al., 2004; Brocca et al., 2009). It is also a limiting factor in crop production and/or vegetational restoration in arid and semi-arid regions, such as the Chinese Loess Plateau (Hu et al., 2009, 2010). Most recent studies have emphasized soil moisture at shallow depths (Starks et al., 2006; Cosh et al., 2008; Brocca et al., 2009; Zhao et al., 2010; Zhang and Shao, 2013), but some, for example Gao and Shao (2012b), have studied the temporal stability of soil–water storage (SWS) in soil layers as deep as 3 m. Wang et al. (2010) investigated the dynamic characteristics of dried soil layers within profiles 6 m deep on the Loess Plateau. Obtaining soil–water data is more difficult for deep than for shallow soils. The characteristics of hydrological processes in deep soil and the relationships with plants, soil properties, and topography are thus relatively poorly known but are necessary for the application and verification of hydrological models (Western et al., 2002; Koster et al., 2004). Information characterizing the soil–water dynamics in various layers is also helpful for developing hydrological models for monitoring water, especially in areas with deep soils.

Soil–water content varies in both space and time due to the heterogeneity and combinations of the controlling factors. The storage of soil water, however, can present persistent spatial patterns over time (Grayson and Western, 1998; Cassel et al., 2000; Mohanty and Skaggs, 2001; Lin, 2006; Brocca et al., 2009, 2010;
Zhao et al., 2010). Vachaud et al. (1985) first introduced this phenomenon as the temporal stability of SWS. Many studies have subsequently examined the temporal stability of soil water for various land uses (Vachaud et al., 1985; Lin, 2006; Jia and Shao, 2013; Liu and Shao, 2014), climatic areas (Jacobs et al., 2004; Hu et al., 2009, 2010), scales (Gao and Shao, 2012a,b; Hu et al., 2010), and topographies (Grayson et al., 2002; Hébrard et al., 2006). Temporal stability can be recognized as similarities of spatial patterns of soil water along time series. Similarly, the persistence of a spatial pattern of soil water along a depth series has been termed depth persistence. Little information about the similarity or persistence of SWS spatial patterns at various depths over time, however, is available for the Loess Plateau. Further investigation of the relationships among the soil–water contents in various layers in this semiarid area would improve our understanding of the vertical soil–water dynamics.

The Loess Plateau of China is known for its uniquely deep loessial soil, intense soil erosion, and degradation of the vegetation (Hu et al., 2009, 2010). It is characterized by many deep gullies and undulating loessial slopes, which produce highly spatially variable soil–water contents (Hu et al., 2009; Wang et al., 2012). The wet (growing) and dry (non-growing) seasons in this region are clearly separated (Jia et al., 2012), and the different conditions of wetness can differentially affect hydrological processes (Vachaud et al., 1985; Lin, 2006; Gao et al., 2011). For example, Gao et al. (2011) found that the temporal stability of spatial patterns of soil water in the root-zone in jujube orchards was higher in either the dry or wet season than for both seasons together. Lin (2006) showed that the temporal stability of soil water varied between dry-down and wet-up periods in complex terrains. The spatial patterns of SWS profiles can differ between the growing and non-growing seasons due to differences in the vegetation and soil wetness. Few reports, however, have addressed these differences on the semiarid Loess Plateau with its complex terrains, soil types, and plant covers. Furthermore, plant growth can also control SWS spatial patterns, because the root structure and vegetation cover affect the evapotranspiration and storage of water (Zhao et al., 2010; Jia and Shao, 2013). Jia et al. (2013a,b) showed that the temporal stability of hillslope-scale SWS profiles was strongly controlled by aboveground biomass and litterfall in a small watershed on the Loess Plateau. The type of vegetation can also significantly affect the temporal stability of soil–water spatial patterns (Jia and Shao, 2013).

Spearman's rank correlation analysis is widely used to identify overall similarity at measurement scale. Kachanoski and de Jong (1988), however, found that the spatial patterns of SWS were scale-dependent for hydrological processes operating at different spatial scales. Wavelet coherency based on wavelet transformation has thus been used to determine the correlations between two variables at different scales and locations, because it can resolve the variability of the data in the spatial series. For example, Biswas and Si (2011c) used wavelet coherency to study the scale- and location-specific temporal stability of SWS between sampling occasions in a hummocky area. Wavelet coherency has also been used to examine the scale- and location-specific variations between two soil properties (Si and Zeleke, 2005; Yates et al., 2007; Biswas and Si, 2011b). The spatial patterns of SWS between surface and subsurface soils on the Loess Plateau, however, have not been analyzed using wavelet coherency. The specific objectives of the present study were thus (1) to investigate the spatial patterns of SWS within profiles along a 1340-m transect in a typical semiarid catchment on the Loess Plateau and (2) to assess the dependence of the similarities of the spatial patterns of SWS on soil depth and season. The overall and scale-dependent similarities of the spatial patterns of SWS were identified using Spearman's rank correlation and wavelet coherency analyses, respectively.

2. Materials and methods

2.1. Study area

The study was conducted in the Liudaogou watershed (110°21'-110°23'E, 38°46'-38°51'N) in Shennu County on the northern Loess Plateau of China (Fig. 1). The study area covers 6.89 km² and is in the transitional belt between the Loess Plateau and the Mu Us desert. The landform is undulating with an elevation of 1056–1130 m a.s.l. The climate is moderate semiarid with a mean annual temperature of 8.4 °C and a mean annual rainfall of 437 mm, more than 70% of which falls from June to September (Fig. 2). According to the growth of vegetation, the entire year can be divided into growing season (from May to October) and non-growing season (from November to April). The primary soil types are Aeolian sandy soils and Ust-Andic Entisols soils. The dominant vegetation includes purple alfalfa (Medicago sativa L.), Korshinsk peashrub (Caragana korshikii Kom.), and bunge needlegrass (Stipa bungeana Trin.). A representative sampling transect with 135 locations at regular intervals of 10 m (Fig. 1) was established in July 2012 in an east–west direction for sampling areas with the dominant soil types, landforms, and vegetation. An aluminum neutron-probe access tube was installed at each location for measuring soil–water content at 15 depths. For most sampling locations, soil–water content can be measured to the maximum depth of 3.0 m. However, soil moisture data for a few sampling locations can only be derived to a depth of 1.2 m due to the presence of bedrock below that depth.

2.2. Sampling and measurements

2.2.1. Measurement of SWS

Soil–water contents were measured with a neutron probe (Beijing Super Power Company, Beijing, China) at each location from 23 August 2012 to 28 October 2013. Samples were measured on 22 occasions during the study period, and we analyzed the data from four randomly selected sampling occasions for both the growing and non-growing seasons. Twelve locations with different water conditions were selected to establish calibration curves following procedure introduced by Hu et al. (2010). Volumetric soil–water content, \( \theta \), was calculated using the calibration equation:

\[
\theta = 0.6565CR - 0.0068 \quad (R^2 = 0.9031, \quad P < 0.001) \quad (1)
\]

where \( CR \) is the slow-neutron counting rate.

Following Jia and Shao (2013), SWS at a specific depth can be calculated as:

\[
S = \theta \times h \times 2 \times 10 \quad (2)
\]

where \( S \) is the SWS at a specific depth (mm), \( \theta \) is the volumetric water content at this depth (cm³/cm³), and \( h \) is the soil-depth interval (20 cm).

2.2.2. Measurement of other soil parameters

Sampling locations and the corresponding site elevations were determined by a GPS receiver with a 5-m resolution. Undisturbed soil samples for measurements of saturated soil hydraulic conductivity (Ks) using the constant-head method (Klute and Dirksen, 1986) and of soil bulk density were collected at each sampling location 0.2 m from the access tube using a cutting ring 5 cm in height. Disturbed soil samples were divided into two sub-samples and air-dried. One sub-sample was passed through a 0.25-mm sieve for the determination of soil organic-carbon (OC) content by the dichromate oxidation method (Nelson and Sommers, 1982). The other sub-sample was passed through a 1-mm sieve to analyze soil-particle sizes using a Mastersizer2000.
In September 2013, we measured peak aboveground biomass clipped from a 1 m quadrat at each location. The plant samples were oven-dried at 75 °C for 72 h to obtain dry weights. Detailed data of the topsoil (0–20 cm), terrain, and vegetational characteristics along the transect are summarized in Table 1.

### 2.3. Assessment of the depth persistence of spatial patterns of SWS

#### 2.3.1. Spearman's rank correlation

The Spearman's rank correlation test was first introduced to identify the similarity of the overall spatial pattern of soil–water...
components of can be expressed as: 

$$g_i = \sum_{j=1}^{n} (R_{ij} - R_{ij}^2)$$

(3)

where $R_{ij}$ and $R_{ij}^2$ are the ranks of the SWS observed at location $i$ in soil layers $j$ and $j'$, respectively, and $n$ is the number of observations. A higher $r_c$ within a series of soil–water measurements indicates a higher degree of similarity between the locations. That is, the closer $r_c$ is to 1, the more similar the spatial pattern (Vachaud et al., 1985).

2.3.2. Wavelet coherency analysis

Wavelet coherency can identify the similarity of spatial patterns between two spatial series. It requires the calculation of a wavelet coefficient for both data series. Wavelet coefficients are identified using wavelet transformation at different scales and locations. Farge (1992) and Kumar and Fouloua-Georgiou (1997) provide detailed introductions describing wavelet transformation, and Grinsted et al. (2004) and Si and Zeleke (2005) describe wavelet coherency. We will present a basic procedure for obtaining wavelet coherency.

The wavelet coefficient, $W_i^s(t)$, is calculated using a continuous wavelet transformation (CWT) for a SWS series of length $n$ ($Y_i$, $i = 1, 2, 3, \ldots, n$) with equal incremental distance $\Delta x$. The CWT can be defined as the convolution of $Y_i$ with the scaled and normalized wavelet with the fast Fourier transformation (FFT) (Torrence and Compo, 1998):

$$W_i^s(t) = \sqrt{\frac{\Delta x}{\pi}} \sum_{j=1}^{n} Y_i \psi[j-i\Delta x/s]$$

(4)

where $\psi[j]$ is the mother wavelet function and $s$ is the scale. $W_i^s(t)$ can be expressed as $a + ib$ where $a$ and $b$ are the real and imaginary components of $W_i^s(t)$, respectively.

There are many types of mother wavelet functions. Among these, Morlet wavelet retaining the real and imaginary components of the wavelet coefficient allows the detection of both location-dependent amplitude and phase for different frequencies in the spatial series (Torrence and Compo, 1998) and can be expressed as:

$$\psi(t) = \pi^{-1/4} e^{i \omega t - 0.5 \eta^2}$$

(5)

where $\omega$ is the dimensionless frequency and $\eta$ is the dimensionless space ($\eta = s/\Delta x$). The Morlet wavelet ($\omega = 6$) is good for extracting features, because it provides a good balance between space and frequency localization.

The cross wavelet power spectrum at scale $s$ and location $i$ for two SWS spatial series $X$ and $Y$, respectively, are calculated as:

$$|W_i^X(s)| = |W_i^Y(s)|$$

(6)

where $W_i^X(s)$ and $W_i^Y(s)$ are the wavelet coefficients of SWS spatial series $X$ and $Y$, respectively, and $W_i^Y(s)$ is the conjugate of $W_i^X(s)$.

The wavelet coherency of two spatial series can be written as (Grinsted et al., 2004; Torrence and Webster, 1999):

$$R_i^s = \frac{|S(s^{-1}W_i^X(s))|^2}{S(s^{-1}|W_i^X(s)|^2)}$$

(7)

where $S$ is a smoothing operator and can be written as:

$$S(W) = S_{scale}(S_{space}(W(s, \tau)))$$

(8)

where $\tau$ indicates location, $S_{scale}$ indicates smoothing along the wavelet scale axis and $S_{space}$ indicates smoothing in spatial distance. The following smoothing function is the normalized real Morlet wavelet and has a similar footprint to the Morlet wavelet. The smoothing along locations thus can be expressed as:

$$S_{space}(W(s, \tau)) = \sum_{i=1}^{n} \left( W(s, \tau) \frac{1}{s^2 \pi^{1/2} 2^{2}} \exp \left( -\frac{(\tau - x_n)^2}{2s^2} \right) \right)$$

(9)

where $\frac{1}{s^2 \pi^{1/2} 2^{2}} \exp (-\frac{\tau^2}{2})$ is the smoothing function, and $\exp(-2s^2\omega^2)$ is the Fourier transformation of this function, where $\omega$ is the frequency (Si and Zeleke, 2005). Eq. (9) can be implemented with FFT and inverse FFT (IFFT) in terms of convolution theorem and then written as:

$$S_{space}(W(s, x)) = IFFT(FFT(W(s, \tau)) \exp(-2s^2\omega^2))$$

(10)

The smoothing along the scales can thereby be written as:

$$S_{scale}(W(s_i, x)) = \frac{1}{2m + 1} \sum_{j=k-m}^{k+m} S_{space}(W(s_j, x) \prod_i (0.6s_j))$$

(11)

where $\prod_i$ is the rectangle function, and $m$ is the number of terms on each symmetrical half of the window. The factor 0.6 is the empirically determined scale decorrelation length for the Morlet wavelet (Si and Zeleke, 2005; Torrence and Compo, 1998).

2.3.3. Significance testing

The significance of the wavelet coherency can be tested against Gaussian white and red noise (Pardo-Iguzquiza and Rodriguez-Tovar, 2000). For white noise, the spatial data series have independently and identically distributed datapoints that are not auto-correlated. For red noise, however, the points have values similar to those of nearby points, but dissimilar to those further apart (Biswas and Si, 2011b). Red noise is thus generally modeled as a univariate lag-1 auto regressive (AR1) process (Torrence and Compo, 1998; Si and Farrell, 2004). Many soil properties, though, commonly exhibit red-noise-like behavior (Si and Farrell, 2004), such as soil–water content, Ks, and OC content. We treated red-noise-like behavior as the assumed background for statistical testing. Our null hypothesis was thus that the wavelet coherency of a measured soil–water series was not different from that of red noise.

For a given AR1 process with a lag-1 autocorrelation coefficient $r$, Monte Carlo simulation was used to generate 1000 realizations of one soil–water series, and the wavelet coherency of each realization was calculated. Therefore, 1000 wavelet coherency values were sorted into ascending order. The 950th wavelet coherency value at a scale and location gives the 95% confidence level at that scale and location (Si and Zeleke, 2005). Unlike Pearson correlations, the wavelet coherency can reflect relationships between variables at each scale and location rather than the overall relationship. The phase information in a wavelet coherency analysis can identify different relationships (such as positive or negative) at each scale and location.

Exploratory analysis was performed in Microsoft Office Excel (Microsoft Corporation Inc., Redmond, USA). Spearman's rank correlation analysis was performed with SPSS 16.0 (SPSS Inc., Chicago, USA). Wavelet coherency analysis was conducted using the MATLAB (The MathWorks Inc., Natick, USA) code written by Grinsted et al. (2004) and available at: http://www.pol.ac.uk/home/research/waveletcoherence/.

3. Results

3.1. Spatial patterns of SWS in the various soil layers

During the non-growing season, SWS had similar spatial patterns among the soil depths along the transect (Fig. 3). Each
layer had several strong peaks along the transect. These peaks were concentrated near the three gullies on the transect but also on slopes, such as at locations 590, 980, and 1270 m on the transect (Fig. 3). The SWS in the 0–20 cm layer on 21 January 2013 during the non-growing season ranged from 10.34 to 68.99 mm, with a mean of 31.77 mm. The mean SWS increased slightly from 31.77 mm in the 0–20 cm layer to 32.85 mm in the 20–40 cm layer and then gradually decreased to 27.27 mm in the 100–120 cm layer (Table 2). The standard deviation (SD) of the SWS ranged from 11.12 mm in the 100–120 cm layer to 13.97 mm in the 40–60 cm layer. The coefficient of variation (CV) of the SWS ranged from 39% in the 0–20 cm layer to 44% in the 60–80 cm layer. The data from other sampling dates during the non-growing season produced similar trends (Table 2). During the growing season, SWS had a similar spatial pattern in each layer, with some peaks along the transect (Fig. 3). These peaks were at the same places on 29 August 2013 as the peaks during the non-growing season (Fig. 3). The mean SWS increased from 33.45 mm in the 0–20 cm layer to 34.90 mm in the 20–40 cm layer and then decreased gradually to 28.47 mm in the 100–120 cm layer (Table 3). The SD of the SWS was very similar in each layer, ranging from 0.62 to 0.97 during the growing season, with means of 0.85 and 0.83, respectively. The mean SWS during the growing season, however, had increased from 16.34 mm in the 0–20 cm layer to 25.12 mm by 15 June 2013 (Table 3). Compared with measurements on 29 August 2013, the mean SWS showed a similar trend on 30 July 2013 and 28 September 2013.

### 3.2. Similarity in the overall spatial pattern of SWS in the various layers

The Spearman’s rank correlation coefficients identified an overall similarity of spatial patterns of SWS among the layers. The coefficients between every pair of depths for any sampling date were statistically significant ($P < 0.01$), indicating strong similarity in the spatial pattern of SWS between layers. $r_s$ decreased with increasing depth interval during both the non-growing (Table 4) and the growing (Table 5) seasons. $r_s$ ranged from 0.71 to 0.95 during the non-growing season and from 0.62 to 0.97 during the growing season, with means of 0.85 and 0.83, respectively.

### 3.3. Similarities in the scales of spatial pattern of SWS in the layers

Wavelet coherency analysis investigated the scale-specific correlations of SWS between the 0–20 cm layer and the other three layers. We divided the scales into three groups using the

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**Table 2**

| Layer (cm) | Max (mm) | Min (mm) | Mean (mm) | SD (mm) | CV (%) |
|-----------|----------|----------|-----------|---------|--------|
| 21 January 2013 | | | | | |
| 0–20 | 68.99 | 10.34 | 31.77 | 12.53 | 39 |
| 20–40 | 73.40 | 10.14 | 32.85 | 13.59 | 41 |
| 40–60 | 80.30 | 8.80 | 32.23 | 13.97 | 43 |
| 60–80 | 71.10 | 7.46 | 30.11 | 13.30 | 44 |
| 80–100 | 61.90 | 8.23 | 28.50 | 12.11 | 43 |
| 100–120 | 63.62 | 7.27 | 27.27 | 11.12 | 41 |
| 24 February 2013 | | | | | |
| 0–20 | 68.22 | 8.61 | 31.64 | 12.36 | 39 |
| 20–40 | 77.80 | 10.14 | 32.87 | 13.79 | 42 |
| 40–60 | 77.80 | 9.95 | 32.11 | 13.80 | 43 |
| 60–80 | 78.00 | 7.46 | 30.15 | 13.85 | 46 |
| 80–100 | 68.99 | 8.80 | 28.61 | 12.66 | 44 |
| 100–120 | 63.52 | 7.65 | 26.98 | 11.32 | 42 |
| 18 March 2013 | | | | | |
| 0–20 | 70.52 | 7.84 | 27.44 | 12.42 | 45 |
| 20–40 | 81.07 | 10.91 | 31.85 | 13.71 | 43 |
| 40–60 | 81.07 | 10.53 | 31.53 | 13.45 | 43 |
| 60–80 | 78.38 | 6.69 | 29.62 | 13.36 | 45 |
| 80–100 | 65.52 | 8.80 | 28.36 | 12.37 | 44 |
| 100–120 | 60.55 | 7.08 | 26.71 | 11.25 | 42 |
| 16 April 2013 | | | | | |
| 0–20 | 52.70 | 5.93 | 21.01 | 10.72 | 51 |
| 20–40 | 60.94 | 10.34 | 28.42 | 12.03 | 42 |
| 40–60 | 71.86 | 8.99 | 29.71 | 12.28 | 41 |
| 60–80 | 70.52 | 6.69 | 28.58 | 12.39 | 43 |
| 80–100 | 63.05 | 9.19 | 28.04 | 11.73 | 42 |
| 100–120 | 61.70 | 7.84 | 26.85 | 11.17 | 42 |
similarities among the wavelet coherency graphs between any two depths for selected measurements. The three scale groups were small (<40 m), intermediate (40–160 m), and large (>160 m), respectively.

Table 3
Statistical summary of soil–water storage in the various layers for a measurement series during the growing season. SD, standard deviation; CV, coefficient of variation.

| Layer (cm) | Max (mm) | Min (mm) | Mean (mm) | SD (mm) | CV (%) |
|------------|----------|----------|-----------|---------|--------|
| 15 June 2013 |          |          |           |         |        |
| 0–20       | 36.98    | 4.01     | 16.34     | 7.08    | 43     |
| 20–40      | 47.33    | 4.97     | 19.48     | 8.37    | 43     |
| 40–60      | 51.16    | 5.54     | 22.05     | 10.11   | 46     |
| 60–80      | 59.21    | 5.93     | 23.68     | 11.39   | 48     |
| 80–100     | 62.66    | 6.12     | 25.12     | 11.89   | 47     |
| 100–120    | 62.85    | 6.69     | 25.12     | 11.22   | 45     |
| 30 July 2013 |        |          |           |         |        |
| 0–20       | 59.79    | 7.84     | 34.08     | 13.30   | 39     |
| 20–40      | 66.88    | 11.29    | 37.51     | 13.15   | 35     |
| 40–60      | 67.07    | 10.53    | 35.54     | 12.30   | 35     |
| 60–80      | 69.95    | 5.16     | 32.42     | 12.89   | 40     |
| 80–100     | 67.45    | 10.14    | 29.96     | 13.03   | 43     |
| 100–120    | 68.03    | 10.14    | 28.20     | 12.13   | 43     |
| 29 August 2013 |      |          |           |         |        |
| 0–20       | 60.17    | 8.80     | 33.45     | 12.53   | 37     |
| 20–40      | 65.54    | 11.29    | 34.90     | 12.61   | 36     |
| 40–60      | 65.73    | 10.14    | 33.23     | 12.51   | 38     |
| 60–80      | 64.96    | 7.84     | 31.06     | 12.87   | 41     |
| 80–100     | 67.26    | 9.76     | 29.81     | 12.97   | 44     |
| 100–120    | 66.69    | 9.76     | 28.47     | 12.44   | 44     |
| 28 September 2013 |    |          |           |         |        |
| 0–20       | 63.43    | 7.27     | 33.50     | 14.29   | 43     |
| 20–40      | 70.14    | 10.34    | 39.30     | 14.67   | 37     |
| 40–60      | 68.22    | 9.76     | 41.08     | 14.89   | 36     |
| 60–80      | 69.95    | 8.80     | 40.50     | 15.34   | 38     |
| 80–100     | 71.48    | 9.57     | 39.82     | 15.16   | 38     |
| 100–120    | 75.12    | 10.14    | 37.53     | 14.58   | 39     |

Table 4
Spearman’s rank correlation coefficients between the soil–water storages of the various layers during the non-growing season.

| Layer (cm) | 0–20 | 20–40 | 40–60 | 60–80 | 80–100 | 100–120 |
|------------|------|-------|-------|-------|--------|---------|
| 21 January 2013 | 1.00 | 0.91  | 0.79  | 0.77  | 0.76   | 0.73    |
| 20–40      | 1.00 | 0.90  | 0.85  | 0.83  | 0.85   | 0.78    |
| 40–60      | 1.00 | 0.95  | 0.89  | 0.85  | 0.85   | 0.85    |
| 60–80      | 1.00 | 0.94  | 0.89  | 0.85  | 0.85   | 0.85    |
| 80–100     | 1.00 | 0.95  | 0.89  | 0.85  | 0.85   | 0.85    |
| 100–120    | 1.00 | 1.00  | 1.00  | 1.00  | 1.00   | 1.00    |
| 24 February 2013 | 1.00 | 0.89  | 0.78  | 0.77  | 0.75   | 0.71    |
| 20–40      | 1.00 | 0.91  | 0.87  | 0.84  | 0.77   | 0.71    |
| 40–60      | 1.00 | 0.95  | 0.88  | 0.82  | 0.82   | 0.82    |
| 60–80      | 1.00 | 0.94  | 0.89  | 0.83  | 0.83   | 0.83    |
| 80–100     | 1.00 | 0.94  | 0.89  | 0.83  | 0.83   | 0.83    |
| 100–120    | 1.00 | 1.00  | 1.00  | 1.00  | 1.00   | 1.00    |
| 18 March 2013 | 1.00 | 0.91  | 0.80  | 0.79  | 0.77   | 0.73    |
| 20–40      | 1.00 | 0.90  | 0.87  | 0.84  | 0.78   | 0.78    |
| 40–60      | 1.00 | 0.95  | 0.89  | 0.83  | 0.83   | 0.83    |
| 60–80      | 1.00 | 0.94  | 0.89  | 0.83  | 0.83   | 0.83    |
| 80–100     | 1.00 | 0.94  | 0.89  | 0.83  | 0.83   | 0.83    |
| 100–120    | 1.00 | 1.00  | 1.00  | 1.00  | 1.00   | 1.00    |
| 16 April 2013 | 1.00 | 0.92  | 0.81  | 0.80  | 0.75   | 0.73    |
| 20–40      | 1.00 | 0.91  | 0.88  | 0.84  | 0.78   | 0.78    |
| 40–60      | 1.00 | 0.95  | 0.88  | 0.82  | 0.82   | 0.82    |
| 60–80      | 1.00 | 0.94  | 0.88  | 0.82  | 0.82   | 0.82    |
| 80–100     | 1.00 | 0.95  | 0.88  | 0.82  | 0.82   | 0.82    |
| 100–120    | 1.00 | 1.00  | 1.00  | 1.00  | 1.00   | 1.00    |

All correlations were significant at $P < 0.001$.

![Fig. 4. Wavelet coherency of soil–water storage along the transect between (a) the 0- to 20 and the 20- to 40 cm layers, (b) the 0- to 20 and the 60- to 80 cm layers, and (c) the 0- to 20 and the 100- to 120 cm layers on 18 March 2013, representing the non-growing season. The y-axes are the scales. The color bars indicate the values of the wavelet coefficients, the solid black lines represent the 5% significance levels, and the arrows indicate the phase relationships. (For interpretation of the references to color in this figure legend, the reader is referred to the web version of this article.)](image-url)
On 18 March 2013 during the non-growing season, SWSs between the 0–20 cm and the other layers, including the 60–80 and 100–120 cm layers, were significantly correlated at small scales at several locations (Fig. 4). SWSs between the 0–20 and 20–40 cm layers were significantly correlated at the intermediate scales across most of the transect, but correlations between the 0–20 and 100–120 cm layers were significant at limited locations (Fig. 4). For the scales of 160–320 m, SWSs were significantly correlated between the 0–20 cm and the other layers along the transect (Fig. 4). On 29 August 2013 during the growing season, SWSs between the 0–20 cm and the deeper layers were significantly correlated at small scales at several locations (Fig. 5). For the intermediate scales, SWSs were significantly correlated across most of the transect between the 0–20 and 20–40 cm layers but only at some locations between the 0–20 cm and the deeper (60–80 and 100–120 cm) layers (Fig. 5). SWSs between the 0–20 cm and the other three layers were significantly correlated along the entire transect at scales of 160–320 m (Fig. 5). The correlations of SWS between the 0–20 cm and the deeper layers at all scales along the entire transect were more similar for the growing than the non-growing season. The spatial patterns of SWS between the 0–20 cm and the deeper layers were similar for the other sampling dates during the non-growing and growing seasons.

We examined the wavelet coherency of SWS spatial patterns at the same layers between the two seasons (data for 18 March and 29 August 2013) (Fig. 6). Significantly correlated locations covered most of the transect intermittently at the small scales. Many locations of the transect were significantly correlated between seasons at the intermediate scales for the 0–20, 60–80, and 100–120 cm layers in addition to locations between 300 and 700 m along the transect (Fig. 6). The SWSs were significantly correlated between seasons along the entire transect for the 20–40 cm layer at the intermediate scales and for all layers at large scales (Fig. 6). The wavelet coherency of SWS spatial patterns at the same layers between other selected dates during growing and non-growing seasons showed the similar results.

The areas of significant correlations indicated the differences in wavelet coherency between the layers during the growing and non-growing seasons. The total area of significant correlation at the different scales generally decreased with increasing depth interval in both seasons (Figs. 4 and 5). The total area representing significant correlation between the same layers was higher for 18 March 2013 than 29 August 2013. The total area of significant correlation between the same layers in the different seasons, however, increased from the 0–20 to the 20–40 cm layer and then decreased with depth (Fig. 6). The directions of the wavelet coherency arrows in Figs. 7 and 8 indicate the type of correlation. Arrows pointing to the right of significant areas suggest an “in phase” relationship, or positive correlation. Arrows pointing to the left indicate an “out of phase” relationship, or negative correlation. SWS was thus correlated negatively with site elevation (Fig. 7) and positively with clay content (Fig. 8).
4. Discussion

SWS fluctuated along the transect in each layer during both the non-growing and growing seasons. SWS had an obvious depth persistence within the profiles (Fig. 3). SWS peaked at different locations along the transect in the different seasons. The presence of peaks in the gullies, indicating the retention of more soil water, may be attributed to the position of the gullies in the landscape. Gullies always act as sinks in this semiarid area, accumulating water from hillslope runoff. The peaks in SWS on the slopes may be due to the soil texture. These locations may contain higher clay contents (Fig. 8). The similar trend of SWS along the profiles in the non-growing season indicated a higher temporal stability of SWS, but SWS varied among different sampling dates in the growing season. More than 70% of the annual precipitation falls in the growing season (Fig. 2), so the water is redistributed unevenly on the undulating landscape. The soil layers thus displayed different water statuses on different sampling dates. Plants, though, consume more than 70% of the water they need from the root zone (Feddes et al., 1978; Morris, 2006), which affects the soil–water dynamics. The SD and CV were similar among the layers, perhaps due to the similar meteorological conditions, topography, and soil texture. In addition, the CVs were moderately variable, based on the scale of Nelsen and Bouma (1985).

The overall spatial patterns between any two SWS series on selected sampling dates during different seasons were strongly similar, in accordance with the observations by Biswas and Si (2011a), Gao and Shao (2012a) and Jia et al. (2013b), perhaps because the soil layers had similar intrinsic soil properties such as texture and OC content or because the layers at the same location had similar hydrological conditions, such as infiltration, runoff, and evapotranspiration. In addition, the correlation coefficients decreased with distance between layers in both seasons. These results are in agreement with those from other studies (Arya et al., 1983; Tallon and Si, 2004; Pachepsky et al., 2005; Guber et al., 2008; Penna et al., 2009; Hu et al., 2009). The effects of climatic conditions (Hu et al., 2010), root activity (Cassel et al., 2000), and soil structure (Guber et al., 2003) on the SWS spatial patterns gradually decrease with depth. Other studies investigating the temporal stability of SWS spatial patterns using Spearman’s rank correlations have reported similar results (Biswas and Si, 2011a; Gao and Shao, 2012b; Jia and Shao, 2013; Zhang and Shao, 2013). For example, Zhang and Shao (2013) found that soil-surface water content was more highly correlated between sampling series collected over a short period of time than over longer periods.

The significant coherency at all scales among the layers in the different seasons may be attributed to the soil texture. The significant scale dependence of SWS on clay content, especially at large scales, is shown in Fig. 8. Hu and Si (2013) and She et al. (2013) also found strong correlations between SWS and clay content using multivariate empirical mode decomposition at larger scales. They attributed these correlations to the higher influence of particle size on SWS at larger scales. The difference in elevation along the transect was large (1056–1130 m), but SWS was not significantly correlated with site elevation, except at a few locations at small scales (Fig. 7). These results did not agree with those by Biswas and Si (2011a). Biswas and Si (2011a) found a significant relationship between SWS and elevation in a hummocky landscape, even though the difference in elevation was <5 m. Knolls and depressions in hummocky landscapes can retain soil water

![Fig. 7. Wavelet coherency between soil–water storage and site elevation (SE) along the transect for the (a and c) 0–20 and (b and d) 100–120 cm layers on (a and b) 18 March 2013 and (c and d) 29 August 2013. The top panels show site elevation (SE) along the transect. The y-axes are the scales. The color bars indicate the values of the wavelet coefficients, the solid black lines represent the 5% significance levels, and the arrows indicate the phase relationships. (For interpretation of the references to color in this figure legend, the reader is referred to the web version of this article.)](image-url)
well, so terrain factors that can affect wavelet coherency between soil layers consist mainly of variations in landform elements and microtopography. The total area of significant coherency at the different scales in our study generally decreased between surface and subsurface layers with increasing depth interval for the different seasons (Figs. 4 and 5). These results indicated a reduction in the degree of depth persistence in SWS spatial patterns and supported the results of the Spearman’s rank correlation analysis. Biswas and Si (2011a) also found that the similarity gradually decreased with distance between the surface and subsurface layers for both recharge and discharge periods. The decrease in our study in the total area of significant coherency from the non-growing to the growing season suggested a reduction in the degree of depth persistence (Figs. 4 and 5), perhaps due to the use of water by the vegetation and/or to the higher precipitation in the growing season, which could affect important hydrological processes, such as evapotranspiration and infiltration, and could change the water storage along the soil profile. The total areas of significant correlation between the same layers in different seasons were large, indicating a high range of SWS temporal stability from the non-growing to the growing season, in agreement with the findings by Biswas and Si (2011c) and Hu et al. (2014). Hu et al. (2014) found that a temporally stable location for estimating the mean SWS in a season of one year could be applied to the same season of another year. The area of significant correlation between the 0–20 and 20–40 cm layers in our study was larger than that between the 0–20 and 100–120 cm layers during the same season (Figs. 4 and 5). In contrast, the area of significant correlation between the 0–20 cm layers between seasons was not significantly different from that of other layers (Fig. 6). We may thus conclude that soil depth had a larger effect than season on the similarities in SWS spatial patterns.

The depth persistence in the SWS spatial patterns between the surface and deeper layers can be used to estimate soil–water content in deeper layers. Measuring the water content only in the surface soil would reduce costs and resources (Biswas and Si, 2011a) and would also provide information necessary for adopting data-assimilation techniques for integrating remote sensing and soil–water modeling (Houser et al., 1998; Walker et al., 2001; Heathman et al., 2003). The depth persistence of SWS within soil profiles could also be incorporated into hydrological models, be applied to water management, and contribute to our understanding of the hydrological dynamics of landscapes.

5. Conclusions

We investigated the similarities in SWS spatial patterns between surface and deeper soil layers during different seasons using Spearman’s rank correlation and wavelet coherency analyses. The following conclusions can be drawn.

(1) Spatiotemporal analysis showed that the temporal evolution of SWS profiles differed between the growing and the non-growing seasons due to the complex effects of controlling factors such as soil texture, terrain, vegetation, and climate.
(2) Significant correlations were observed between any two soil layers during both seasons, and the correlation coefficients decreased with distance between layers.

(3) The significant coherency of SWS spatial patterns between layers may be attributed to clay content at large scales during different seasons.

(4) The total area of significant coherency decreased from the non-growing to the growing season, suggesting a reduction in the degree of depth persistence. Soil depth had a higher effect than season on the depth persistence of the SWS spatial patterns.

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