To bend a coralline: effect of joint morphology on flexibility and stress amplification in an articulated calcified seaweed

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SUMMARY

Previous studies have demonstrated that fleshy seaweeds resist wave-induced drag forces in part by being flexible. Flexibility allows fronds to ‘go with the flow’, reconfiguring into streamlined shapes and reducing frond area projected into flow. This paradigm extends even to articulated coralline algae, which produce calcified fronds that are flexible only because they have distinct joints (genicula). The evolution of flexibility through genicula was a major event that allowed articulated coralline algae to grow elaborate erect fronds in wave-exposed habitats. Here we describe the mechanics of genicula in the articulated coralline Calliarthron and demonstrate how segmentation affects bending performance and amplifies bending stresses within genicula. A numerical model successfully predicted deflections of articulated fronds by assuming genicula to be assemblages of cables connecting adjacent calcified segments (intergenicula). By varying the dimensions of genicula in the model, we predicted the optimal genicular morphology that maximizes flexibility while minimizing stress amplification. Morphological dimensions of genicula most prone to bending stresses (i.e. genicula near the base of fronds) match model predictions.

Key words: adaptation, biomechanics, Calliarthron, decalcification, drag, flexibility, geniculum, intertidal, macroalgae, material properties, modulus.

INTRODUCTION

Researchers have long studied morphological adaptations that allow intertidal macroalgae to survive the hydrodynamic forces imposed by breaking waves (e.g. Delf, 1932; Koehl, 1986; Carrington, 1990; Dudgeon and Johnson, 1992; Friedland and Denny, 1995; Blanchette, 1997; Gaylord, 1997; Bell, 1999; Denny and Gaylord, 2002; Boller and Carrington, 2006; Harder et al., 2006). One unifying characteristic that has been thoroughly explored in these studies is flexibility. By being flexible, macroalgae ‘go with the flow’, limiting drag forces by reducing the thallus area projected into rapid flow, reconfiguring into more streamlined shapes, and bending over into slower moving water (Koehl, 1986; Gaylord and Denny, 1997; Denny and Gaylord, 2002; Boller and Carrington, 2006). Thus, for plants and algae growing in habitats characterized by unstable flow, flexibility is not only considered adaptive (Vogel, 1984) but is also generally regarded as a ‘pre-requisite for survival’ (Harder et al., 2004).

Unfortunately, because fleshy macroalgae probably evolved from fleshy (flexible) ancestors, adaptive hypotheses are difficult to test; flexibility may be a matter of default, rather than of design. In contrast, coralline algae (Corallinales, Rhodophyta) are firmly calcified and have a fossil record that extends back hundreds of millions of years (Johnson, 1961; Wray, 1977; Steneck, 1983). According to this fossil record, about 100 million years ago, coralline algae evolved articulations, called genicula, that gave flexibility to calcified fronds (Johnson, 1961; Wray, 1977; Steneck, 1983). This evolutionary innovation allowed coralline algae to grow away from unstable flow, reconfiguring into more streamlined shapes, and bending over into slower moving water (Koehl, 1986; Gaylord and Denny, 1997; Denny and Gaylord, 2002; Boller and Carrington, 2006). Thus, for plants and algae growing in habitats characterized by unstable flow, flexibility is not only considered adaptive (Vogel, 1984) but is also generally regarded as a ‘pre-requisite for survival’ (Harder et al., 2004).

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some species, such as the coralline Calliarthron cheilosporioides Manza (Fig. 1A), often dominating wave-exposed low-intertidal habitats.

Despite the ecological and mechanical success of articulated coralline algae, the mechanics of articulated fronds are poorly understood. While fleshy algae are flexible along the entire length of their thallii, the flexibility of articulated coralline algae is confined to discrete positions along otherwise rigid thalli. The effect of this distinct segmented morphology on bending performance and stress amplification is an open question.

Genicula in the articulated coralline Calliarthron are composed of thousands of elongated cells (Martone, 2007). The distal ends of each flexible genicular cell remain firmly calcified and embedded in adjacent intergenicula (Johansen, 1969, Johansen, 1981), thereby tethering intergenicula together. Moreover, unlike cells in most plant tissues, adjacent genicular cells are only loosely connected to one another. Genicular cells fray and separate as genicula break (P.T.M. and M.W.D., unpublished observations), possibly due to minimal and weak middle lamella between cells. These qualities suggest that a Calliarthron geniculum may be modeled not as a single solid but, rather, as a collection of straight cables capable of sliding past one another with minimal shear resistance.

In this study, we describe the geometry of bending genicula and introduce a computational model that utilizes genicular geometry to predict deflections of articulated fronds. By varying genicular dimensions in the model, we tested the effect of articulated frond morphology on flexibility and genicular stress amplification. We predicted optimal genicular dimensions that maximize flexibility (thereby reducing drag force) while minimizing stress (thereby reducing risk of breakage), and tested whether genicula subject to the greatest bending stresses (i.e. those nearest frond bases) adhered to our predictions.
MATERIALS AND METHODS

Genicular geometry

The morphology of Calliarthron genicula is illustrated in Fig. 1. Genicula have initial length $l_0$, are separated by calcified intergenicula of length $L$, and are bounded laterally by intergenicula lips of length $x$ (Fig. 1B). Fronds are generally flattened, branching in two dimensions, and genicula are elliptical in cross-section with major radius $r_1$ and minor radius $r_2$ (Fig. 1C). Because flexural stiffness is proportional to the cube of bending radius (Wainwright et al., 1982), genicula are presumed to be more flexible when bent over the shorter minor radius (i.e. around the longer major radius). We assume genicula always bend around $r_1$, as fronds reorient under breaking waves. Genicula are circumscribed by elliptical intergenicula with minor radius $y$ (Fig. 1C). Genicula and intergenicula are assumed to be concentric.

Measuring tensile modulus ($E_t$)

Determining the stiffness or tensile modulus ($E_t$) of genicular tissue was central to modeling the mechanics of genicular bending. Fifteen Calliarthron fronds were collected from the low-intertidal zone in a moderately wave-exposed surge channel at Hopkins Marine Station in Pacific Grove, CA, USA. The field site was identical to that described previously (Martone, 2006; Martone, 2007). In each trial ($N=15$), a frond was secured between the grips of a custom-made tensometer (see Martone, 2006), allowing several genicula and genicula to ‘float’ between the grips. Paper tabs were glued to the two intergenicula flanking a single unflawed geniculum near the base of each experimental frond. The tensometer pulled fronds apart at 1 mm s$^{-1}$, while a video dimension analyzer measured the distance between the paper tabs under a dissecting microscope. In this manner, applied force ($\pm 0.002$ N) and change in genicular length ($\pm 0.6$ $\mu$m) were measured concurrently. Extension was continued until fronds broke. Stretched genicula were freshly cross-sectioned with a razor blade, and initial cross-sectional areas were calculated by measuring the inner diameters ($\pm 27$ $\mu$m) of the circumscribing calcified tissue, which is unaffected by genicular deformation, using an ocular dial-micrometer. One geniculum neighboring each experimental geniculum was long-sectioned and its length ($\pm 27$ $\mu$m) was measured using the ocular dial-micrometer. Standard deviation of genicular length was low ($<7\%$ of the mean), and stretched genicula were assumed to be identical in length to neighboring genicula. Nominal stress (force/unstretched cross-sectional area) versus engineer’s strain (change in length/initial length) was plotted for one experimental geniculum in each frond. Tensile moduli ($E_t$) were calculated as the slopes of linear stress–strain regressions forced through the origin. Mean $E_t$ ($N=15$) was used in the bending model described below.

Bending model

Deflections of articulated fronds were modeled numerically. Complete details of the bending model are included in Appendix A. In brief, breaking waves apply drag force, $F$, in the direction of flow, parallel to the substratum and perpendicular to initial frond orientation. At each geniculum, drag generates external bending moments that are resisted by internal moments within genicular tissue. By setting external and internal moments equal to one another, we calculated angles, $\phi$, to which genicula must bend to attain equilibrium and, thereby, estimated frond deflections. This study focused on the basal-most 10 genicula – where bending was expected to be greatest – and drag was simplified to be a downstream force applied to the end of the tenth intergenicula (Fig. 2). 

Testing the bending model

Ten Calliarthron fronds were collected from the field site described above. Branches were removed from each frond by cutting below the first dichotomy, and the remaining straight chains of segments (generally the first 10–20 genicula) were tested as follows. For each trial, fronds were gripped by the first few genicula in clamps and held horizontal; consequently, the first three to five genicula in each test frond were hidden within the clamps and were not tested here. A thread lasso was tied and glued around the eleventh geniculum.
Estimating maximum stress

As articulated fronds bend, basal genicula experience the greatest bending moments and the greatest bending stresses. After predicting deflections of articulated fronds, the numerical model estimated the maximum stress within the first genicula of our sampled fronds based on genicular morphology and bending angles. Mathematics describing these stress calculations are provided in Appendix B.

Effect of genicular characteristics on stress and flexibility

The computational model was used to evaluate the effects of genicular dimensions on (1) frond flexibility, inferred from the deflection angle of entire fronds, calculated as arctan (x-coordinate/y-coordinate) of the frond tip relative to the frond base, and (2) maximum stress within first (basal) genicula. Mean values for genicular dimensions were calculated from all Calliarthron genicula bent in the 10 trials (t0, N=27; all other dimensions, N=100) and were assumed to be constant along a virtual ‘average’ frond. Data for the average frond were entered in the bending model and tested at F=0.2 N. Holding all other dimensions constant at their mean values, each dimension (t0, x, E, y, L, r1 and r2) was varied independently and the resulting frond deflections were recorded. To explore the overall effect of genicular radius, r1 and r2 were varied concurrently and in the same proportion. When intergenicular length was varied, the number of intergenicula was adjusted to hold overall frond length constant (e.g. half as many intergenicula, twice as long as the mean). In one trial, genicular dimensions were all held constant but tensile modulus was allowed to vary. Because hypothetical values of some dimensions were limited by others (e.g. intergenicula could not be longer than half the length of genicula, genicular radii could not be broader than intergenicular radii), the hypothetical range of each dimension differed, so each dimension was experimentally varied in different proportions. Frond flexibility and maximum stress were quantified in each trial, and percentage change (from average) in flexibility and stress were plotted against percentage change (from average) in genicular dimensions. The ratio of percentage change in flexibility (a potential benefit) to percentage change in stress (a potential cost) was plotted against percentage change of each genicular dimension. This benefit:cost index was used to explore changes in genicular dimensions that would increase flexibility or decrease stress and thereby improve bending performance. Shifts in genicular dimensions that increased the benefit:cost index were assumed to be beneficial, while shifts that decreased the index were assumed to be detrimental. Hypothetical genicular dimensions were assumed to be ‘optimal’ if they were positioned at critical points along benefit:cost index curves, such that further change in that dimension, positive or negative, decreased the benefit:cost ratio.

Optimal genicular morphology

Results from the flexibility/stress analysis were used to predict dimensions of genicula optimized for bending. Genicula that experience the most bending (hereafter called ‘bending’ genicula; e.g. genicula no. 1 and no. 2, nearest the base) and genicula that experience little bending and mostly tension (hereafter called ‘tensile’ genicula; e.g. genicula no. 11 and no. 12, farther from the base) were compared in 10 Calliarthron fronds collected from the field site described above. Genicula and intergenicular radii were measured in cross-sections of genicula no. 1 and no. 11, and genicular length, intergenicular length and intergenicular lip length were measured in decalcified long-sections of genicula no. 2 and no. 12 as described above. Student’s paired t-tests were used to compare characteristics of bending and tensile genicula.
RESULTS
Tensile modulus
Stress–strain curves were approximately linear (Fig. 3). Mean tensile modulus of genicular tissue was 27.7±6.8 MN m$^{-2}$ (mean±95% confidence interval, CI).

Bending model
The bending model predicted articulated frond deflections with reasonable accuracy (Fig. 4). In general, real and predicted angles of first genicula were similar at all test forces (Table 1). At the lowest force ($F=0.05$ N), slight over-prediction of bending angles near the base of the fronds caused slight over-prediction of frond deflections. Error in predicting deflection angles decreased with increasing force. At the greatest applied force ($F=0.98$ N), the bending model predicted frond deflections within 1–2 deg. (Table 1).

Effect of genicular characteristics on stress and flexibility
Average genicular dimensions are listed in Table 2. Adjustments to genicular dimensions had varying effects on average frond deflections (Fig. 5). Increasing all genicular dimensions increased frond stiffness, except for increasing genicular length, which decreased frond stiffness (Fig. 5A). Decreasing genicular length by 25% and increasing intergenicular length by 400% made fronds the most stiff (Fig. 5A,D). Increasing tensile modulus had little effect on overall frond stiffness. For example, increasing intergenicular length and intergenicular radius by 100%, increasing genicular radii by 50%, and increasing intergenicular lip length at 25% had greater effects on frond stiffness than quadrupling tensile modulus (Fig. 5).

Adjustments to genicular dimensions had varying effects on flexibility and stress (Fig. 6). As genicular length increased and as genicular radii, intergenicular lip length and tensile modulus decreased, flexibility increased while stress cycled between decreasing and increasing trends (Fig. 6A–C,F). As intergenicular length and intergenicular radius increased, flexibility decreased while stress increased (Fig. 6D,E).

Contrasting effects of genicular dimensions on frond deflections and stress within first genicula were accounted for by plotting the benefit:cost ratio of flexibility to stress (Fig. 7). Increasing genicular length or decreasing intergenicular lip length, or increase in genicular dimensions had varying effects on average frond deflections. Instead, the model presented here treats genicula not as solids but as assemblages of independent cables (genicular cells) with zero shear resistance (see details in Appendix A) – although the presence of some slight shear resistance may explain why the model initially over-predicts deflections at low strains. The similarity of real and predicted frond deflections reported here suggests that genicular cells may, indeed, behave like separate elements sliding past one another, potentially a structural adaptation for increasing flexibility.

Under breaking waves, articulated corallines bend, reorient and go with the flow. This drag-induced bending can lead to mechanical

**DISCUSSION**

**A simple bending model**

Despite their superficial simplicity, *Calliarthron* genicula are complex structures. They are composed of loosely connected cells that interact through a middle lamella of unknown composition and with unknown shear resistance. The cells produce cell walls that vary in composition and structure through time and across individual genicula (Martone, 2006; Martone, 2007). Moreover, these dynamic structures are surrounded by calcified intergenicular lips that may grind down, deform or break when genicula bend. Nevertheless, the geometric model described here estimates frond deflections with reasonable success, allowing for a detailed analysis of articulated frond performance.

Many studies have modeled the bending of biological structures using standard beam theory (e.g. Koehl, 1977; Vogel, 1984; Denny, 1988; Niklas, 1992; Etnier, 2003). For example, erect seaweeds, such as stipitate kelps, are thought to deform like cantilevered beams (Koehl, 1986; Denny, 1988; Gaylord and Denny, 1997). Our early attempts to model genicula as solid beams under-predicted frond deflections. Instead, the model presented here treats genicula not as solids but as assemblages of independent cables (genicula cells) with zero shear resistance (see details in Appendix A) – although the presence of some slight shear resistance may explain why the model initially over-predicts deflections at low strains. The similarity of real and predicted frond deflections reported here suggests that genicular cells may, indeed, behave like separate elements sliding past one another, potentially a structural adaptation for increasing flexibility.

Under breaking waves, articulated corallines bend, reorient and go with the flow. This drag-induced bending can lead to mechanical

| Force (N) | Angle of first geniculum | Deflection of frond tip |
|----------|--------------------------|------------------------|
|          | Mean (deg.) | Mean predicted (deg.) | Mean (deg.) | Mean predicted (deg.) | Difference (deg. ± 95% CI) | Difference (deg. ± 95% CI) |
| 0.05     | 19.1        | 23.3           | 5.1±3.3     | 55.0        | 72.1           | 17.1±4.9   |
| 0.20     | 28.5        | 29.6           | 5.0±1.7     | 70.6        | 78.9           | 8.3±3.2    |
| 0.98     | 46.0        | 37.8           | 8.7±4.0     | 82.1        | 82.5           | 1.3±0.7    |

Table 1. Error in predicting angles of first genicula and deflection of frond tips (N=10)
failure, as articulated fronds are sometimes cast ashore having broken at basal genicula (Martone, 2006). Our data suggest that frond flexibility and the amplification of stress within genicula are both affected by variation in genicular dimensions. Increasing flexibility presumably benefits articulated fronds by decreasing thallus area projected into flow and by increasing reconfiguration, thereby decreasing drag, but may also increase stress. Increasing tissue stress negatively affects algae by increasing the likelihood of breakage. Adjustments to genicular dimensions that increase the ratio of flexibility to stress can be considered net benefits for articulated fronds and potential adaptations to drag-induced bending. These adjustments are described below.

### Morphological adaptations to bending articulated fronds

#### Long genicula

According to the computational model, lengthening genicula makes fronds more flexible and, up to a point, reduces tissue stress – two qualities that benefit articulated fronds. Thus, it is reasonable to hypothesize that long genicula are adaptations to bending. This hypothesis is supported by patterns of genicular development and variation in genicular length along individual fronds. *Calliarthron* genicula consist of a single tier of cells that elongate as they develop (Johansen, 1969; Johansen, 1981). Mature genicular cells are nearly 100 times longer than they are wide (see Martone, 2007) and are approximately 10 times longer than adjacent calcified cells in the intergeniculum (Johansen, 1969). Furthermore, genicula near the bases of fronds – here called ‘bending’ genicula because they probably experience the most bending – tend to be longer than genicula further up the frond (Table 3).

This hypothetically adaptive growth pattern may be both biologically and mechanically limited. *Calliarthron* genicular cells lose cytoplasm and organelles as they elongate and may, therefore, be developmentally incapable of growing any longer. Furthermore, data generated by our computational model suggest that, beyond some critical length, elongating genicula may increase tissue stress (Fig. 6A), limiting the selective pressure to lengthen. This non-linear trend in tissue stress reflects the subtle numerical interaction between genicular length (\(\omega\)), bending angle (\(\phi\)), and intergenicular contact angle (\(\beta\); see Eqn A32 in Appendix B).

#### Short intergenicular lips

Similar in effect to lengthening genicula, shortening intergenicular lips makes fronds more flexible and initially reduces tissue stress (Fig. 6C). However, our data suggest that, below some critical length, reducing intergenicular lip length may increase tissue stress. Fine-tuning of intergenicular lips to minimize tissue stress may occur in reality, as intergenicular lip length changes dynamically over time. Calcified lips initially form when genicula decalcify, thereby separating adjacent intergenicula. The remaining intergenicular tissue becomes meristematic, recovering from the effects of localized decalcification, and calcified lips grow toward one another. At the same time, calcified lips abrade and grind one another down as fronds bend in the field (Johansen, 1981). Thus, the length of intergenicular lips is self-adaptive, depending upon two antagonistic processes: growth and abrasion. Morphological data support the model conclusions; intergenicular lips of bending genicula are indeed significantly reduced (Table 3), but are not completely absent.

### Table 2. Mean genicular dimensions used in bending model analysis

| Dimension                          | Mean (mm) ± 95% CI |
|------------------------------------|--------------------|
| Genicular length, \(\omega\)        | 0.57±0.02          |
| Major genicular radius, \(r_1\)     | 0.57±0.02          |
| Minor genicular radius, \(r_2\)     | 0.46±0.02          |
| Intergenicular lip length, \(x\)    | 0.20±0.01          |
| Intergenicular length, \(L\)        | 3.31±0.16          |
| Intergenicular radius, \(y\)        | 0.69±0.02          |

\(\omega\), \(N=27\); all other dimensions, \(N=100\).
Short intergenicula

Shortening intergenicula makes fronds more flexible by increasing the spatial density of joints along articulated fronds. The effect of joint density on stiffness has been documented for other segmented biological beams (e.g. Etnier, 2001). As a consequence of greater flexibility, shorter intergenicula reduce the lever arm of applied forces, which lowers the moment and stress in bending genicula. Thus, shortening intergenicula both minimizes stress and maximizes flexibility. This adaptive hypothesis is borne out within individual fronds: intergenicula separating bending genicula near frond bases are significantly shorter than those separating more distal tensile genicula (Table 3). Unlike intergenicular lip length, which may fluctuate with growth and abrasion, intergenicular length is likely to be under strict biological control: shorter intergenicula probably consist of fewer (or shorter) tiers of calcified cells laid down during development. Whether intergenicular length is a plastic response to wave-induced bending stresses is unknown, but subtidal Calliarthron, which probably experience less drag, may be able to persist with longer intergenicula, although preliminary comparisons of articulated

Table 3. Morphological differences among bending and tensile genicula

|                  | Bending genicula | Tensile genicula | P-test |
|------------------|------------------|------------------|--------|
| Genicular length (mm) | 0.59±0.04        | 0.55±0.04        | P=0.08 |
| Major genicular radius (mm) | 0.55±0.05        | 0.56±0.05        | n.s.   |
| Minor genicular radius (mm) | 0.48±0.04        | 0.49±0.08        | n.s.   |
| Intergenicular lip length (mm) | 0.08±0.03        | 0.19±0.03        | P<0.001|
| Intergenicular length (mm) | 1.35±0.14        | 3.77±0.70        | P<0.001|
| Intergenicular radius (mm) | 0.67±0.07        | 0.70±0.07        | n.s.   |

N=10 pairs; mean ± 95% CI; n.s., not significant.

Fig. 5. Effect of varying genicular dimensions on frond deflection. (A) Genicular length, ω, (B) genicular radii \( r_1 \) and \( r_2 \), (C) intergenicular lip length \( x \), (D) intergenicular length \( L \), (E) intergenicular radius \( y \) and (F) tensile modulus, \( E_t \).
Mechanics of bending coralline algae

Fronds collected from different habitats suggest little site-to-site variation in intergenicular length.

Taken to its logical conclusion, this adaptive hypothesis suggests that articulated fronds should have infinitely short intergenicula to experience none of the disadvantages of segmentation. Such seaweeds would resemble fleshy macroalgae. That intergenicula are not infinitely short suggests that complete decalcification might be disadvantageous. For example, calcification minimizes the impact of herbivores on coralline fronds (Steneck, 1986; Padilla, 1993). Alternatively, there may be some metabolic cost associated with decalcification, suggesting a trade-off between energy allocation and biomechanical performance. The observed density of joints in Calliarthron may reflect the least number of joints sufficient to reduce stress, increase flexibility and permit survival of articulated fronds.

Unmodified genicular and intergenicular radii

According to the computational model, decreasing genicular radii and increasing intergenicular radii greatly increase tissue stress (Fig. 6B,E). Conversely, increasing genicular radii and decreasing intergenicular radii have minor effects on flexibility. As a result, substantial change in either radial dimension negatively affects articulated fronds (Fig. 7). Thus we would not expect to find adaptive shifts in genicular or intergenicular radii within bending genicula. As expected, neither radial dimension was significantly different among bending and tensile genicula (Table 3).

Interestingly, although the radii of the basal 10 genicula are generally similar, genicular radii decline measurably from base to tip within Calliarthron fronds (Martone, 2006). Slender, more distal, genicula are unlikely to experience much bending, but rather resist drag on distal segments in tension. Thus, reduced genicular radius is not necessarily maladaptive in these distal genicula. On the contrary, thinner genicula support fewer segments in flow and, therefore, are subject to less drag; the smallest (most apical) genicula may be over-designed for this purpose (Martone, 2006).

Decreased tensile modulus

According to the model, a slight decrease in tensile modulus would increase flexibility and reduce tissue stress (Fig. 6F). However, anything beyond a slight decrease would drastically increase stress, potentially limiting the selective pressure to reduce the tensile modulus. For example, either decreasing or increasing the tensile modulus by 50% has comparable effects on the benefit:cost ratio (Fig. 7). Calliarthron genicular tissue is actually quite stiff compared

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**Fig. 6.** Effect of varying genicular dimensions on the maximum stress within first genicula (triangles) and the deflection angle of whole fronds (circles). X-axes represent percentage change in (A) genicular length \( \omega \), (B) genicular radii \( r_1 \) and \( r_2 \), (C) intergenicular lip length \( x \), (D) intergenicular length \( L \), (E) intergenicular radius \( y \) and (F) tensile modulus \( E_t \). Note that axes have differing scales.

**Fig. 7.** Effect of varying genicular dimensions on the ratio of flexibility (a presumed benefit) to stress (a presumed cost). Adjustments to genicular dimensions that increased the flexibility:stress ratio were considered net benefits for articulated fronds. Symbols represent changes in genicular radii (black circles), genicular length (black triangles), intergenicular lip length (black squares), intergenicular length (gray circles), tensile modulus (gray triangles) and intergenicular radius (gray squares).
with several other algal tissues (Hale, 2001). But genicular tissue can also resist greater stresses than other algal tissues (Martone, 2006). The ‘strong and stiff’ breakage strategy of genicular tissue can be contrasted with the ‘weak and stretchy’ strategy of other seaweed tissues (Koehl, 1984; Koehl, 1986; Hale, 2001). Ultimately, the distinct combination of strength and stiffness allows genicula to absorb and resist more than 10 times the energy per volume imposed by breaking waves as that resisted by many other seaweeds (Hale, 2001). Consequently, *Calliarthron* genicula can remain moderately stiff without risking frond breakage.

**APPENDIX A**

**Bending model details**

Frond deflections are resisted by the genicula separating each calcified segment (Fig. A1). Fronds reach equilibrium when external and internal moments are equal.

**External moments**

Given drag force, $F$, applied in the downstream direction perpendicular to an erect frond, we can calculate bending moment, $M$, as:

$$M = F\delta,$$  \hfill (A1)

where $\delta$ is the lever arm, the distance from force application to the center of any bending geniculum (Fig. 2A). As fronds bend, lever arms decrease (Fig. 2B). Ultimately, the reduction in lever arm is a function of total bending angle at each geniculum. For example, in Fig. 2:

New $\delta_1 = L_1\cos(\phi_1) + L_2\cos(\phi_1 + \phi_2) + L_3\cos(\phi_1 + \phi_2 + \phi_3)$.

$$\delta_1 = L_1\cos(\phi_1) + L_2\cos(\phi_1 + \phi_2) + L_3\cos(\phi_1 + \phi_2 + \phi_3).$$  \hfill (A2)

**Internal moments**

The total internal moment $M$ resisted by any geniculum is the sum of elemental moments:

$$M = \int dM = \int z dF,$$  \hfill (A3)

where internal moments, like external moments, are the products of forces and lever arms. In this case, elemental moments, $dM$, are the result of elemental forces, $dF$, applied some distance, $z$, away from the neutral axis of the geniculum. The neutral axis is the position within genicula that remains unstressed during bending.

Given the definition of tissue stress $\sigma$:

$$\sigma = \frac{F}{A},$$  \hfill (A4)

it follows that:

$$F = \sigma A,$$

$$dF = \sigma dA,$$  \hfill (A5)

where $A$ is unstretched genicular cross-sectional area, and any elemental force, $dF$, can be expressed as the product of stress and elemental area, $dA$ (see Fig. A2). Thus, $M$ can be expressed by substituting for $F$:

$$M = \int z \sigma dA.$$  \hfill (A6)

Given that tissue stiffness $E$ is defined as:

$$E = \frac{\sigma}{\varepsilon},$$  \hfill (A7)

$$\sigma = E \varepsilon,$$

where $\varepsilon$ is tissue strain, we can substitute for $\sigma$ to yield:

$$M = \int z E \varepsilon dA.$$  \hfill (A8)

Using elliptical polar coordinates, we describe positions along the genicular periphery by:

$$a = r_1\cos\theta,$$

$$b = r_2\sin\theta,$$  \hfill (A9)

where $\theta$ is the angle relative to the geniculum center (Fig. A2). Taking the derivative of the $y$-coordinate:

$$db = r_2\cos\theta d\theta.$$  \hfill (A10)

The area of any elemental rectangular portion of ellipse is:

$$dA = (2a)db = 2r_1 r_2 \cos^2 \theta d\theta.$$  \hfill (A11)
Substituting Eqn A10 into Eqn A8, total internal moment can be expressed as:

\[
M = \int_{-\frac{\pi}{2}}^{\frac{\pi}{2}} z E \epsilon r_2 \cos^2 \theta d\theta .
\] (A12)

At this point, we use this equation in two distinct ways to separate the two sequential modes of geniculum bending that occur before and after adjacent intergenicula make contact.

**Moments before intergenicula make contact**

Before adjacent intergenicula touch, genicula are bent such that all tissue on the upstream side of the neutral axis is stretched via tension, while all tissue on the downstream side of the neutral axis is squeezed via compression (Fig. A3). By definition, the neutral axis remains unstressed during bending, does not change length, and is located some perpendicular distance, \( \eta \), away from the genicular midline. The position of the neutral axis depends upon tensile \( (E_t) \) and compressive \( (E_c) \) moduli, such that moments within tensile and compressive halves are balanced and no net force results. When tensile and compressive moduli are equivalent, the neutral axis passes directly through the center of the tissue. However, tensile and compressive moduli of biological materials are often not equal. Gaylord (Gaylord, 1997) demonstrated that for several kelp tissues:

\[
E_t = 4E_c .
\] (A13)

Here this conclusion is applied to genicular tissue. Tensile moduli are measured experimentally, and then compressive moduli are assumed to be 4 times lower. The result is an off-center neutral axis, shifted toward the tensile side of genicula (Fig. A3).

Using \( E_t \) and \( E_c \), we can calculate the exact location of the neutral axis by iteratively solving for \( \eta \) in the following equation, derived in appendix 7 of Gaylord (Gaylord, 1997):

\[
\left( E_t - E_c \right) \left( \frac{r_2^2 - \eta^2}{3} + \frac{\eta r_2^2}{2} \arcsin \left( \frac{\eta}{r_2} \right) + \frac{\eta^2 r_2^2}{2} \sqrt{r_2^2 - \eta^2} \right) - \left( E_t + E_c \right) \eta r_2^2 \pi = 0 .
\] (A14)

Now we can explicitly define the distance, \( z \), between the neutral axis and any elemental area of genicularium (Fig. A3B) over which elemental forces are applied (Eqns A3–A6):

\[
z = r_2 \sin \theta - \eta .
\] (A15)

Tissue strain, \( \epsilon \), can be calculated from the change in tissue length between intergenicula:

\[
\epsilon_{\text{pre-contact}} = \frac{\omega + \frac{2m}{\omega}}{\omega} - 1 = \frac{2m}{\omega} ,
\] (A16)

where \( m \) is additional length defined by the triangle in Fig. A3A, such that:

\[
\sin \left( \frac{\phi}{2} \right) = \frac{m}{r_2 \sin \theta - \eta} .
\] (A17)

**Fig. A3.** Diagram of bending geniculum in long-section (A) and cross-section (B) before intergenicula make contact. Genicular tissue is shown in yellow; intergenicular tissue is shown in pink; \( m \) is additional length; \( \omega \) is genicular length; \( \eta \) is the perpendicular distance of the neutral axis from the genicular midline; and \( x \) is the intergenicular lip length.

Note that this model assumes that genicula follow the shortest straight line distance between intergenicula, as if composed of cables, and do not curve like a typical bent solid (see Discussion). Substituting for \( m \) in Eqn A16 yields:

\[
\frac{2 \left( r_2 \sin \theta - \eta \right) \sin \left( \frac{\phi}{2} \right)}{\omega} .
\] (A19)

Then substituting for \( \epsilon \) in Eqn A12, we obtain an expression describing the internal moment resisted by genicula bent to angle \( \phi \) before intergenicula make contact:

\[
M = \int_{-\frac{\pi}{2}}^{\frac{\pi}{2}} \left( r_2 \sin \theta - \eta \right) \left( 2 \left( r_2 \sin \theta - \eta \right) \sin \left( \frac{\phi}{2} \right) \right) E \left( \frac{2r_2 \cos^2 \theta d\theta}{\omega} \right) .
\] (A20)

**Intergeniculum contact angle**

When intergenicula first make contact, we can define a contact angle \( (\phi=2\beta) \), described by a triangle that extends from the point of intergenicular contact to the neutral axis (Fig. A4), such that:

\[
\sin \beta = \frac{\omega - 2x}{2y + \eta}.
\] (A21)
Substituting for $k$ in Eqn A24 yields:

$$\varepsilon_{\text{post-contact}} = \frac{2(y + r_2 \sin \phi)\sin \left(\frac{\phi}{2}\right) + 2x}{\omega} - 1.$$  \hspace{1cm} (A27)

To account for tissue strain before intergenicula made contact ($\phi \leq 2\beta$), we combine Eqns A19 and A27 as follows:

$$\varepsilon_{\text{total}} = \varepsilon_{\text{pre-contact}} + \varepsilon_{\text{post-contact}}$$

$$= \frac{2(r_2 \sin \theta - \eta)\sin(\beta)}{\omega} + \frac{2(y + r_2 \sin \phi)\sin \left(\frac{\phi}{2} - \beta\right) + 2x}{\omega}$$

$$= \frac{2(r_2 \sin \theta - \eta)\sin(\beta) + 2(y + r_2 \sin \phi)\sin \left(\frac{\phi}{2} - \beta\right) + 2x}{\omega} - 1.$$  \hspace{1cm} (A28)

Finally substitution for $\varepsilon$ in Eqn A12 yields an expression describing the internal moment resisted by genicula bent to angle $\phi$ after intergenicula make contact:

$$M = \frac{2r_2}{\omega} \left(\frac{2(y + r_2 \sin \phi)}{\omega} + 2 \left(\frac{r_2 \sin \theta - \eta}{\omega}\right)\sin(\beta) + 2x\right)$$

$$= \frac{2r_2 \cos^2 \theta d\theta}{\omega}.$$  \hspace{1cm} (A29)

Implementation of geometry in Matlab

The above geometrical relationships were incorporated into a Matlab routine in order to predict the deflection of articulated fronds by applied forces. In practice, genicular dimensions for 10 genicula and an applied force were inserted into the model. Bending angles (2$\beta$) at which intergenicula make contact were calculated. Moments required to bend genicula before and after intergenicula make contact were calculated by iteratively solving Eqns A20 and A29, respectively, for three arbitrary values of $\phi$ (0.4, 0.8, 1.0), using $E=E_c$ for negative strains and $E=E_r$ for positive strains. Linear regressions were fitted to the two sets of three ($M, \phi$) datapoints and were subsequently used to quickly calculate $\phi$ for genicula given applied moments.

The model initially applied a small fraction (1/100) of the total force at the frond apex and calculated external moments at all genicula (Eqns A1 and A2; Fig. 2). Moments were used to calculate bending angles at all genicula, using the linear regression described above, assuming intergenicula had not yet made contact. Lever arms were re-calculated, given the bending angles (Eqn A2), force was incremented, and external moments were re-calculated at all genicula (Eqns A1 and A2). Moments were used to calculate new bending angles, using ‘after contact’ linear regressions if previous angles exceeded 2$\beta$. Bending angles and incremented force were used to re-calculate lever arms and external moments, and new angles were calculated using moment regressions. This process was repeated until maximum force was applied.
The model computed maximum stress (i.e. stress in the outermost yellow; intergenicular tissue is shown in pink; section (B) after intergenicula make contact. Genicular tissue is shown in genicular tissue.

Increasing stress.

Tensile stresses were generally one to two orders of magnitude less than bending stresses in this study, but become increasingly important as fronds bend to 90 deg. Note that once fronds reach 90 deg. (the maximum bending angle, $\phi_1$), additional increases in $\phi$ increase $\beta$ and drive tissue stress down.

Genicular length

Slight increases in $\phi$ decrease stress, but as $\phi$ continues to increase, $\phi_1$ increases rapidly as fronds bend over, causing tissue stress to increase (Fig. 6A). Once fronds bend 90 deg. (the maximum bending angle, $\phi_1$), additional increases in $\phi$ increase $\beta$ and drive tissue stress down.

Genicular radius

Increasing $r_1$ and $r_2$ causes a slight decrease in $\phi_1$, a slight increase in other terms (Eqn 32) and, ultimately, has very little effect on stress. Decreasing $r_1$ and $r_2$ causes $\phi_1$ to increase rapidly, increasing tissue stress (Fig. 6B). Once fronds bend to 90 deg., further reduction in $r_2$ causes stress to decline.

Intergenicular lip length

Decreasing $x$ initially has little effect on $\phi_1$, but causes stress to decrease. Further decreases in $x$ cause $\phi_1$ to increase rapidly, increasing stress.

Tensile modulus

Decreasing $E_t$ initially causes tissue stress to decrease, but eventually causes $\phi_1$ to increase, driving stress back up.

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