Massive black holes in high-redshift Lyman Break Galaxies

M.C. Orofino, A. Ferrara, S. Gallerani

Scuola Normale Superiore, Piazza dei Cavalieri 7, I-56126 Pisa, Italy

ABSTRACT

Several evidences indicate that Lyman Break Galaxies (LBG) in the Epoch of Reionization (redshift $z > 6$) might host massive black holes (MBH). We address this question by using a merger-tree model combined with tight constraints from the 7 Ms Chandra survey, and the known high-$z$ super-MBH population. We find that a typical LBG with $M_{\text{UV}} = -22$ residing in a $M_h \approx 10^{12} M_\odot$ halo at $z = 6$ host a MBH with mass $M_\bullet \approx 2 \times 10^8 M_\odot$. Depending on the fraction, $f_{\text{seed}}$, of early halos planted with a direct collapse black hole seed ($M_{\text{seed}} = 10^5 M_\odot$), the model suggests two possible scenarios: (a) if $f_{\text{seed}} = 1$, MBH in LBGs mostly grow by merging, and must accrete at a low ($\lambda_E \approx 10^{-4}$) Eddington ratio not to exceed the experimental X-ray luminosity upper bound $L_X = 10^{42.5}$ erg s$^{-1}$; (b) if $f_{\text{seed}} = 0.05$ accretion dominates ($\lambda_E \approx 0.22$), and MBH emission in LBGs must be heavily obscured. In both scenarios the UV luminosity function is largely dominated by stellar emission up to very bright mag, $M_{\text{UV}} > -23$, with BH emission playing a subdominant role. Scenario (a) poses extremely challenging, and possibly unphysical, requirements on DCBH formation. Scenario (b) entails testable implications on the physical properties of LBGs involving the FIR luminosity, emission lines, and presence of outflows.

Key words: galaxies: high redshift – galaxies: active – galaxies: evolution

1 INTRODUCTION

The presence of massive black holes (MBH, $M_\bullet \approx 10^7–8 M_\odot$) in typical Lyman Break Galaxies (LBGs) in the Epoch of Reionization (EoR) has become a very pressing question in early galaxy and black hole (co-)evolution. These objects might hold the key to understand at least three fundamental issues: (a) do MBHs in LBGs represent the progenitor population of supermassive black holes (SMBH, $M_\bullet \gtrsim 10^9 M_\odot$) powering the brightest quasars (QSO)? (b) what can we learn about black hole seeds and growth of these compact objects? (c) do they affect, and by what physical mechanisms, the properties and evolution of early galaxies and even large scale structure, e.g., contributing to the reionization and metal enrichment of the intergalactic medium?

At present, we have collected significant statistics and luminosity functions of a large sample of high-$z$ galaxies over a wide span of magnitudes, thanks to space-born surveys, such as (i) the Hubble Ultra Deep Field, and the eXtreme Deep Field, exploiting the power of WFC3 onboard the Hubble Space Telescope (Oesch et al. 2010; Bouwens et al. 2011, 2015; McLure et al. 2015; Bouwens et al. 2017); (ii) the Hubble CLASH lensing surveys (Atek et al. 2015; McLure et al. 2016; Livermore et al. 2017); (iii) X-ray surveys (Sun et al. 2019; Calhau et al. 2020). These endeavours are complemented by a number of ground-based surveys (Bradley et al. 2012; Bowler et al. 2013; Bouwens et al. 2016; Fogasy et al. 2020). Although the detected galaxies are seen within $\sim 1$ Gyr from the Big Bang, some of them have already built-up large stellar masses and appear as evolved systems, containing an almost solar abundance of heavy elements and dust. For recent reviews on these topics we defer the reader to Dayal & Ferrara (2018); Maiolino & Mannucci (2019).

In lower-$z$ galaxies there is evidence for a relation between stellar mass and the massive black holes harbored at their centers (Kormendy & Ho 2013; Heckman & Best 2014; Reines & Volonteri 2016). This connection is not yet fully established at high-$z$. Some cosmological hydrodynamical simulations, such as Horizon-AGN (Volonteri et al. 2016) and BlueTides (Huang et al. 2018) show no significant evolution in the relation up to $z \sim 8$. The same conclusion is found by Marshall et al. (2020) with a semi-analytical model that highlights minimal evolution in the black hole–bulge and black hole–total stellar mass relations out to $z = 8$ (see also Lupi et al. 2019). Other results from hydrodynamical

1 For a comparative study on large scale cosmological hydrodynamical simulations we refer to Habouzit et al. (2020). Such work focuses on the mass properties of SMBH and on their relation with the stellar mass of the host galaxies in six different simulations. It is worth noting that while all the simulations generate a $M_\bullet - M_\ast$ relation in general accordance with observations, some simulations are in tension with the data for low-mass BHs $M_\bullet < 10^{7.5} M_\odot$. 
simulations (Khandai et al. 2012; Barai et al. 2018) and semi-analytical models (e.g. LAMAstra et al. 2010) of $z \sim 6$ SMBHs show deviations from the local relation (Kormendy & Ho 2013). These results seem to be confirmed by a handful of high-$z$ observations (Wang et al. 2010; Targett et al. 2012; Willott et al. 2015; Pensabene et al. 2020) available to date. They show an over-massive black hole trend with respect to the host stellar mass. In particular, the analysis by Targett et al. (2012) at $z \sim 4$ shows a fast growth of the BH-to-stellar mass ratio with redshift as $\propto (1+z)^{1.4-2.0}$. However, these works are still debated and not conclusive. Specifically, Salvianer et al. (2007) concluded that apparent evolution of the local law can be due to observational biases.

Observations are jeopardized by several difficulties. The standard direct X-ray detection of AGN technique, widely applied at lower redshifts, becomes very challenging for these remote and intrinsically faint (or obscured, Trebitsch et al. 2019a; Ni et al. 2020) objects. Fortunately, new results pushing instrumental capabilities to their very limits have been nevertheless obtained: using the 7 Ms Chandra survey (Vito et al. 2018; Cowie et al. 2020) have derived very stringent and useful constraints on the early MBH population. In this paper we will extensively made use of these constraints to calibrate and anchor our models. As the UV emission from MBH is likely swamped by stellar light emitted by the galaxy, observations in this band can be hardly conclusive about the presence of a central black hole in LBGs. Faint Active Galactic Nuclei (AGN) might also be present within Lyman Alpha Emitters (LAE) as recently shown by Calhau et al. (2020) (see also Haro et al. 2020). These authors studied the X-ray and radio properties of about 4000 LAEs at $2.2 < z < 6$ from the SC4K survey in the COSMOS field. They detect 6.8% (3.2%) of these sources in the X-rays (radio). The interpretation of these results relies on the existence of a population of extremely faint/obscure AGN that escape even the deepest X-ray searches, but are potentially detectable in radio emission.

In spite of these difficulties, MBH might be caught by searching for the unique features they imprint on the observed properties of the host galaxy. These indirect probes might then allow us to reliably answer the questions outlined at the beginning. Among other possibilities, there are at least three indirect but clear smoking guns of the presence of a hidden MBH in a LBG.

- Outflows, in turn, might profoundly affect galaxy morphology, star formation, escape of ionizing photons and metal enrichment of the circumgalactic and intergalactic medium. Although at least some of these effects are degenerate with the star formation activity (Dayal et al. 2010; Pizzati et al. 2020) or PopII emission (Palottini et al. 2015), their combination can uniquely pinpoint the presence of a MBH. Furthermore, signatures of outflowing gas have been recently found in several $z > 5$ galaxies (Gallerani et al. 2018; Sugahara et al. 2019; Fujimoto et al. 2019; Ginolfi et al. 2020). These outflows may be possibly powered by a yet undetected accreting MBH.

Here we use available data in combination with simple but robust semi-analytical models, similar to previous works by Tanaka & Haiman (2009); Petri et al. (2012); Tanaka (2014), to study the mass and luminosity of MBH as a function of the host halo mass. With this approach we aim to assess whether LBGs at $z = 6$ host MBH, determining the MBH mass and Eddington ratio and preliminarily appraise their impact on the galaxy properties.

The paper is organized as follow: Sec. 2 describes the merger tree, seeding and growth prescriptions, along with the observational constraints we impose. In Sec. 3 we derive the BH-halo mass relation, and in Sec. 4 we use it to compute the combined galaxy-AGN luminosity function for two different scenarios. Sec. 5 contains the implications for LBGs, including FIR luminosity, emission lines, and presence of outflows. Finally, a summary is given in Sec. 6.

# 2 Method

We run merger trees by using the public code $^3$ described in Parkinson et al. (2008). Our initial goal is the derivation of the relation between the mass of the BH and the host dark matter halo. We generate merger trees with root halos of mass in the range $M_h = 10^{10.6-13} M_\odot$ at $z = 6$. Then we seed the leaves with BHs, and follow their accretion and merging down to the root. Our method is similar to the one used by Tanaka & Haiman (2009), and is best suited to derive the most probable BH mass hosted by a halo of known mass, along with its expected variance.

We specialize our analysis to redshift $z = 6$, where observational data on UV and X-ray luminosity of AGN are available and can provide indirect constraints on the black hole-galaxy relation. Our aim is to study the BH final mass and accretion rate at that epoch, even for those BH masses that are smaller than observed. We then require that the

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$^3$ Throughout the paper, we assume a flat Universe with the following cosmological parameters: $\Omega_M h^2 = 0.1428$, $\Omega_\Lambda = 1 - \Omega_M$, and $\Omega_B h^2 = 0.02233$, $h = 67.32$, $\sigma_8 = 0.8101$, where $\Omega_M$, $\Omega_\Lambda$, $\Omega_B$ are the total matter, vacuum, and baryonic densities, in units of the critical density; $h$ is the Hubble constant in units of $100$ km $s^{-1}$, and $\sigma_8$ is the late-time fluctuation amplitude parameter (Planck Collaboration et al. 2018).

$^4$ star-www.dur.ac.uk/~cole/merger_trees/
combined BH-galaxy luminosity functions satisfy the available constraints from deep UV/X-ray surveys, and use the results to make predictions for future early galaxies observations.

2.1 Merger Tree setup and parameters

Parkinson et al. (2008) algorithm follows the formation history of dark matter halos using the extended Press-Schechter theory. It has been shown to be in accurate agreement with the conditional mass functions found from ΛCDM Millennium N-body simulations. For further details on the code we refer the reader to Parkinson et al. (2008).

We sample 40 different final halo masses equally spaced in log space from $M_{\text{min}} = 10^{10.6} M_\odot$ to $M_{\text{max}} = 10^{13} M_\odot$ and run 100 merger trees for each mass to achieve a significant statistics. The mass resolution of the merger trees is $M_{\text{res}} = 5 \times 10^5 M_\odot$; they follow the cosmic evolution from $z = 30$ to $z = 6$. For each of the trees we computed the BH mass inside the halos, following accretion and merging history from the high-$z$ leaves to the $z = 6$ root. The seeding and accretion prescriptions are described in the following.

2.1.1 Seeding

Seeding prescriptions employing stellar mass BH ($M_\bullet \gtrsim 10^2 M_\odot$) seeds are known to face difficulties in explaining the observed $10^6 M_\odot$ SMBHs at $z = 6$ (Álvarez et al. 2009; Oordino et al. 2018). Such models have to resort to prolonged super-Eddington accretion phases (Madau et al. 2014; Volonteri et al. 2015; Aversa et al. 2015; Lupi et al. 2016; Regan et al. 2019; Takeo et al. 2020). In contrast with models in which radiation pressure regulates gas infall, such as e.g. Park (2012); Park & Ricotti (2013); Toyouchi et al. (2020); Sugimura & Ricotti (2020).

We use instead a seeding prescription based on intermediate mass $M_\bullet \approx 10^5 M_\odot$ black holes (IMBH). These seeds represent the possible outcome of two direct formation scenarios: (i) monolithic collapse of the gas in H$_2$-free primordial halos (direct collapse BH, see, e.g. Recs 1984; Bromm & Loeb 2003; Mayer et al. 2010; Ferrara et al. 2014; Mayer et al. 2015) and (ii) heavy seeds formation in low-metallicity, dense stellar clusters where, due to energy equipartition, the most massive members tend to sink towards the center (Spitzer 1969; Vishniac 1978; Begelman & Recs 1978; Lee 1987; Quinlan & Shapiro 1990; Omukai et al. 2008; Devecchi & Volonteri 2009; Devecchi et al. 2010; Mehrgan et al. 2019; Boco et al. 2020). We refer to Latif & Ferrara (2016); Mezcua (2017) and Inayoshi (2020) for recent reviews on this topic.

Ferrara et al. (2014) studied the IMBH initial mass function and host halo properties. They concluded that a good prescription is to seed halos of mass $7.5 < \log(M_h/M_\odot) < 8$ in the redshift range $8 < z < 17$ with IMBH of mass $4.75 < \log(M_\bullet/M_\odot) < 6.25$. We then adopt this prescription, but for simplicity assume a single $M_\bullet = 10^5 M_\odot$.

We also note that the above results represent only a necessary condition for the formation of IMBH. The prescription implicitly assumes that the halo is illuminated by a sufficiently strong UV Lyman-Werner (11.2–13.6 eV) intensity $J_{LW} > J_{LW}^\ast$ so to prevent molecular hydrogen formation during the collapse. The precise value of the intensity threshold, $J_{LW}^\ast \approx (30–1000) \times 10^{-21}$ erg s$^{-1}$ cm$^{-2}$ Hz$^{-1}$ sr$^{-1}$, depends on radiative transfer, chemistry and spectral shape of the sources, and it is only approximately known (Ferrara et al. 2013; Sugimura et al. 2013, 2015; Agarwal & Khochfar 2015; Agarwal et al. 2016). We condense this uncertainty in the $f_{\text{seed}}$ parameter expressing the fraction of potential host candidate halos that actually meet the above illumination condition, and therefore are seeded with an IMBH.

To summarize our seeding procedure: we planted a seed of $10^5 M_\odot$ in a fraction $f_{\text{seed}}$ of the merger-tree leaves that have mass $7.5 < \log(M_h/M_\odot) < 8$ in the redshift range $8 < z < 17$; $f_{\text{seed}}$ is constant over such mass/redshift ranges. As we will see in Sec. 3, we distinguish two different scenarios: in the first one, all the IMBH host halo candidates are planted with a seed; in the other, only a small randomly selected fraction of the candidates hosts a seed. Different values of the fraction of seeded halos $f_{\text{seed}}$ lead to qualitatively different BH build-up scenarios: $f_{\text{seed}} \approx 1$ implies that the bulk of the BH mass is gained by seed-merging, while in the lower $f_{\text{seed}}$ case the BH mass is mainly gained by direct gas accretion. Note that $f_{\text{seed}}$ is a free parameter of our model.

2.1.2 Growth

Implanted BH seeds can grow via two distinct channels: BH-BH merger and direct gas accretion. We assume that every halo merger results in an instantaneous BH merging. This is justified by previous calculations (Armitage & Natarajan 2006; Volonteri & Rees 2006; Colpi 2014) which showed that coalescence is very rapid due to the fact that both viscous dissipation in the surrounding accretion disk, and energy loss due to gravitational wave emission have timescales much shorter than the Hubble time ($\approx 1$ Gyr) at $z = 6$.

For simplicity, we do not consider gravitational-radiation induced recoil (Merritt et al. 2009; Devecchi et al. 2009; Devecchi et al. 2009) neither. This assumption is partly justified by the findings of Schnittman & Buonanno (2007) indicating that the typical velocities for gravitational recoil (or “kick”) are of the order of 100 km s$^{-1}$.

However, other works (e.g. Tamburello et al. 2017; Pfister et al. 2019; Bortolas et al. 2020) deem these assumptions as too optimistic, as some BHs might be kicked off from the galaxies during the initial growth stages or because the merging time might not be negligibly short. This might lead to an overestimate of the merger efficiency, and hence of the final MBH mass in merging-dominated scenarios. However, as a test, we checked that a random scatter in the seed mass range $(0.2–1.8) \times 10^5 M_\odot$ introduces variations < 5% in the results.
this issue does not affect the results of accretion-dominated scenarios.

In between two merger episodes, we allow BHs to grow by direct accretion at a fraction $\lambda_E$ of their Eddington rate, $M_\bullet = \lambda_E M_\dot{E}$, where

$$M_\dot{E} \equiv \frac{L_\dot{E}}{\eta \epsilon_c^2} = 2.5 \times 10^{-8} \left( \frac{M_\bullet}{M_\odot} \right) \left( \frac{0.1}{\eta} \right) M_\odot \text{yr}^{-1},$$

(1)

where $L_\dot{E} = 1.5 \times 10^{48} (M_\bullet / M_\odot) \text{erg s}^{-1}$ is the Eddington luminosity. The allowed values for the matter-radiation conversion efficiency, $\eta$, range from 0.054 for non-rotating Schwarzschild BHs to 0.42 for maximally rotating Kerr BHs (Shapiro et al. 1983). Following the arguments given in Marconi et al. (2004) we will take $\eta = 0.1$ in the following. The Eddington-ratio $\lambda_E$ is a free parameter of the model, and it is further discussed in the next Sections; in particular, we refer to Sec. 3.1 where the calculation of the Eddington-ratio is summarized.

### 2.2 BH Luminosity

From the assumptions made in the previous Section it follows that the bolometric luminosity of the BH is simply given by

$$L = \lambda_E (M_\bullet) L_\dot{E}.$$  

(2)

In the previous equation we have highlighted the likely possibility that the Eddington ratio is a function of BH mass. This function is not yet specified in our model. In the next Section we will discuss the constraints on $\lambda_E$ descending from available observational data. We will then explore the effects of different $\lambda_E$ prescriptions.

For later use we will need to calculate the X-ray (0.5–2 keV band) and UV (at 1450 Å) luminosity of the black holes. These can be directly obtained from the bolometric luminosity by applying the appropriate bolometric corrections, i.e.

$$L_i = f_i (L) L,$$

(3)

with $L$ given by eq. (2) and $i = X, \text{UV}$. For both $f_X$ and $f_{\text{UV}}$ we use the luminosity-dependent fit by Shen et al. (2020) (see their Fig. 2). For example, for $L = 10^{46} \text{erg s}^{-1}$ they find $f_X = 0.02$ (soft band) and $f_{\text{UV}} = 0.2$, respectively.

### 2.3 Observational constraints

In order to constrain direct accretion efficiency and obscuration (see Sec. 3.2 and Sec. 3.3), we use two types of experimental constraints available at $z \approx 6$. The first one comes from the abundance and luminosity of SMBH. According to $\Lambda$CDM ([Sheth et al. 2001] [Mo & White 2002] [Mo et al. 2010]) and for the adopted cosmology, the comoving density of the most massive halos in our merger tree, $M_{\text{max}} = 10^{12} M_\odot$, at $z = 6$ is $n_{\text{max}} \approx 10^{-9} \text{Mpc}^{-3}$. According to the results of the Sloan Digital Sky Survey ([Jiang et al. 2009]) this abundance corresponds to a UV magnitude (at 1450 Å) in the range $-27 < M_{\text{UV}} < -25$. In this work we will use $M_{\text{UV}} \approx -26$ or $L_{\text{UV}} \approx 2 \times 10^{46} \text{erg s}^{-1}$ or $L \approx 10^{47} \text{erg s}^{-1}$. This sets a constraint on the product $\lambda_E M_\bullet \approx 6 \times 10^4 M_\odot$. As measurements of the virial SMBH mass using MgII line width of individual SDSS sources and other high-$z$ quasars ([Willett et al. 2007] [Kurk et al. 2007] [Mortlock et al. 2011]) indicate $M_\bullet \approx (1-3) \times 10^7 M_\odot$, one can conclude that $\lambda_E \approx 0.2$–0.6 in the supermassive regime.

The second constraint comes from X-ray observations. [Cowie et al. (2020)] searched for high-redshift ($z > 4.5$) X-ray AGN in the deep central region of the 7 Ms Chandra Deep Field-South (CDFs) X-ray image. They put a tight upper limit, $n_X = 10^{-7} \text{Mpc}^{-3}$, on the comoving density of $z \approx 6$ X-ray sources with $L_X > L'_X \approx 10^{42} \text{erg s}^{-1}$ in the 0.5–2 keV band.

Paralleling the previous procedure, this abundance corresponds to a halo mass $M_\bullet \approx 10^{12} M_\odot$. Note that this halo mass scale is typical of the most massive halos in our merger tree, $M_{\text{max}} = 10^{12} M_\odot$, at $z = 6$ LBGs with $M_{\text{UV}} \approx -22$ ([Behroozi et al. 2019] and Fig. 1). CDFs observations then set a constrain $\lambda_E M_\bullet \approx 10^7 M_\odot$ for BH hosted by LBGs at the end of the Epoch of Reionization. We should also allow for the possibility that a fraction of the emitted light by the AGN is absorbed by dust and gas in the vicinity of the black hole. When appropriate, we denote this fraction as $f_{\text{abs}}$ in the appropriate X-ray or UV band.

### 3 CONSTRAINED HALO-BH RELATION

As already mentioned, the seeding prescription we are using (see 2.1.1) represents only a necessary condition for the formation of a IMBH by direct collapse. In fact, not all the candidate host halos might be illuminated by a sufficiently strong LW flux such to prevent H$_2$ formation, leading to detrimental cooling fragmentation during the collapse. Given this uncertainty, we explore in the following two different scenarios, S1 and S2.

- **Maximal seeding** [Scenario S1]. This scenario assumes that all the candidates IMBH host halos are exposed to a sufficiently high LW flux field coming either from a nearby galaxy or the cosmological background. This implies a fraction $f_{\text{seed}} = 1$ of seeded halos in the leafs.
- **Inefficient seeding** [Scenario S2] This scenario envisages an inhomogeneous LW background, as predicted by most studies ([Yue et al. 2014]) in which only a small fraction of the putative host halos can form a IMBH. Guided by these findings, we seed a fraction $f_{\text{seed}} = 0.05$ of the leafs. Due to the likely inhomogeneous topology of the LW background, S2 scenario seems largely favored.

As we will see in the following, the main difference between the two scenarios is the relative importance of merging and accretion for the BH growth. In S1 the bulk of the final MBH mass is already made up by the seeds, and therefore limited accretion is required. In S2, instead, the initial seed mass

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7 The precise value of $n_{\text{max}}$ is somewhat sensitive to the cosmological parameters, particularly $\epsilon_\text{g}$, and the transfer function used. As the primary goal of this work is to study MBH in LBGs, this uncertainty has virtually no impact on our results.

8 We recall that the $L_X$ value is so low that it could be produced purely by High Mass X-ray Binaries and hot ISM in a galaxy forming stars at a rate of $\approx 150 M_\odot \text{yr}^{-1}$ ([Mineo et al. 2014] [Das et al. 2017]; see also Sec. 3.1).
Figure 1. Halo vs massive black hole mass relation at \( z = 6 \). Left panel: Results of the merger tree simulations (blue points) for scenario S1 \( (f_{\text{seed}} = 1) \). Variance of individual points is evaluated from \( \approx 100 \) merger tree realizations performed per halo mass bin. The red line represents the best fit (see text for an analytical expression) to the data. The Eddington ratio, \( \lambda_E \), required to match CDFs and QSO abundance data is shown by the blue line. Also shown is the result of numerical simulations by Costa et al. (2014); Barai et al. (2018); Trebitsch et al. (2020): the predicted trend is consistent with these works, although our BH masses are slightly larger. The bottom panel shows the \( M_*/M_h \) ratio across the halo mass range. Right: Same for S2 \( (f_{\text{seed}} = 0.05) \).

is decreased by 20 times, and therefore growth must occur largely by accretion. We discuss the implications of these two scenarios in the following.

In this work we assume that BHs are active at all times, i.e. we do not introduce a duty cycle; however, we introduce obscuration in model S2 to satisfy the observational constraints. As obscuration and duty cycle are known to be degenerate (Shankar et al. 2010; Chen & Gnedin 2018; Trebitsch et al. 2019b), the two possibilities can be disentangled only with the help from ancillary data such as IR observations or clustering experiments.

3.1 Constraining the Eddington parameter

In this Section we detail the procedure used to compute \( \lambda_E \) in S1 and S2.

- **Model S1.** In this model, growth is dominated by BH seed merging and direct accretion is significant only for SMBHs. We initialize the model with \( \lambda_E = 0 \) and computed BH masses accordingly; \( \lambda_E \) is then constrained for \( 10^{12} M_\odot \) and \( 10^{13} M_\odot \) halos with the observed X-ray luminosity. We find that, with S1 seeding assumptions, accretion is negligible for \( 10^{12} M_\odot \) halos, and it does not significantly affect the final BH mass. However, it becomes important for SMBH. To determine it, we run the model again iteratively with the new values of \( \lambda_E \), linearly interpolated in log-log scale as we explain in Sec. 3.2 At the end of each run, we used the final BH masses to compute the new values of \( \lambda_E \) that comply with the \( L_X \) constraints. We stopped the iteration when the change in LBG and SMBH masses was smaller than simulation variance.

Of course, the simplest prescription would be a constant \( \lambda_E \), but this assumption is not suitable for model S1: indeed, in order to simultaneously comply with both the QSO and the LBG observational constraints, the Eddington-ratio should be relatively high and significant obscuration must be invoked. We remind that in this scenario the bulk of the BH mass is gained by merging and that, without obscuration, the BH masses that we compute are \( \approx 10^{-4} M_h \). Including obscuration and increasing \( \lambda_E \) would lead to much higher final BH masses; most importantly, we would overshoot SMBH masses. Finally, we point out that obscuration is degenerate with \( \lambda_E \) and cannot be constrained independently.

- **Model S2.** In model S2, \( \lambda_E \) is constant. We fix \( \lambda_E \) in order to produce in the most massive halo the same BH mass as in S1. We stress that in this scenario \( \lambda_E \) has to be relatively high to produce the supermassive black holes observed in quasars. This forces the introduction of obscuration in the model, thus justifying the simple prescription of a constant \( \lambda_E \).

Model S1 is an extreme and limiting case of BH accretion modeling as the final BH mass is dominated by seed mergers, and no obscuration has been introduced. In principle, it would be possible to modify the model in other reasonable ways, e.g. by introducing obscuration in LBG galaxies and adjust \( \lambda_E \) accordingly. For simplicity, in this work, we concentrate on the simplest scenarios in which BH growth is either accretion- or merger-dominated. However, most of the implications of our results will be investigated for model S2 which we consider as the fiducial one.

3.2 Maximal seeding scenario

In the S1 scenario \( f_{\text{seed}} = 1 \). Our model in this case predicts a tight, almost linear relation between the MBH and halo mass (Fig. 1), whose best fit is \( \log M_* = -3.4^{+0.1}_{-0.1} + 0.9^{+0.01}_{-0.01} \log M_h \). Note that the variance in the relation, evalu-
uated from the $\approx 100$ merger tree realizations performed per halo mass bin, is very small.

Halos corresponding to typical LBGs at $z = 6$ ($M_h \simeq 10^{12} M_\odot$) are predicted to host BHs with mass $M_\bullet = 2 \times 10^8 M_\odot$. Such ratio, $M_\bullet/M_\star \approx 2 \times 10^{-4}$, is approximately constant in the entire BH mass range, as depicted in the lower panel of Fig. [1]; this value is significantly smaller than the seeding one, $0.001 - 0.03$.

If we convert the halo mass into stellar mass using the models by Behroozi et al. (2019) we obtain $M_\star = 1.3 \times 10^{10} M_\odot$, corresponding to a BH/stellar mass ratio $\mathcal{R} \approx 0.015$. While higher than the local value, $\mathcal{R} = 0.0037$ – see eq. 10 of Kormendy & Ho (2013) – yet this value is consistent with high-z determinations [Wang et al. 2010] [Targett et al. 2012] [Willott et al. 2015]. Although at $z = 6$ the observational relation is affected by a large scatter [Pensabene et al. 2020] and observational bias, our result confirms that BHs grew faster than their host stellar counterpart. These conclusions hold for both S1 and S2.

As $\lambda_E$ governs also the growth of the black hole (d$log M_\bullet \propto \lambda_E$) we impose the SMBH abundance/mass and X-ray luminosity limits according to the deep central region of the 7 Ms CDFs X-ray image (Cowie et al. 2020) into our merger tree by linearly interpolating in log-log space $\lambda_E$ in the halo mass range $10^{12} - 13 M_\odot$. For smaller halos we keep $\lambda_E \equiv$ const. (see Fig. [1]); since this value is very low, $\approx 10^{-3}$, implying a very inefficient accretion, our conclusions are weakly affected by a different assumption on the shape of $\lambda_E$ for halos $M_h \lesssim 10^{12} M_\odot$. We then solve the problem by iteration. The key challenge is to produce the SMBHs powering quasars, at the same time preventing MBHs to become too luminous. $\lambda_E$ affects both $M_\bullet$ and the luminosity (in particular, the X-ray luminosity $L_X$). The higher $\lambda_E$, the higher $L_X$, since $L_X$ is a monotonic function of $\lambda_E$; this function is not analytical, since it depends on the development of the merger-tree, from which we compute $L_X(\lambda_E)$ for any given $\lambda_E$. In particular, it has to be

$$L_X(\lambda_E) = L_X^{\text{obs}},$$

where $L_X^{\text{obs}}$ is the observed luminosity. Such equation is solved for the two $L_X^{\text{obs}}$ values derived from observations of LBGs and QSOs by Cowie et al. (2020) and Jiang et al. (2009), respectively.

The CDFs luminosity limits implies that MBH in LBGs must accrete at a low Eddington ratio $\lambda_E = 3 \times 10^{-3}$; such value must increase to 0.36 to reproduce the quasar constraints. These values imply a somewhat different growth mechanism for MBH and SMBH. Accreted matter represents on average only 5% of the final MBH mass at $z = 6$, the rest being acquired by merging; however, its contribution raises up to 20% for SMBH with mass $M_\bullet = 10^8 M_\odot$. In spite of such (mild) dependence on BH mass, a general conclusion is that accretion is a sub-dominant BH growth channel in S1 as a result of the large number of IMBH seeds available for mergers in this scenario. To gain further insight on this important aspect, we show in Fig. [2] with red lines the growth history of a MBH hosted by a LBG-type halo (left panel), and that for a SMBH (right). For this calculation, we followed the growth history of the seed located in the highest leaf from $z \approx 17$ down to the root. In particular, for each halo our code keeps track of two masses: (i) the mass of the merged seeds, $M_1$, (ii) the mass of directly accreted material, $M_2$. The actual BH mass is the sum of the two, $M_1 + M_2$. At each time-step, we add the mass $M_2$, assuming that accretion occurs at a fraction $\lambda_E$ of the Eddington rate. When a merging event occurs, we sum the two masses, keeping separate track of the two quantities. For example: (a) in a seeded leaf, $M_1 = 10^7 M_\odot$ and $M_2 = 0$; (b) in the final root, $M_1$ is the sum of all the seeds in the merger tree. $M_2$ is the sum of mass accreted by each BH in the tree in all time-steps. In this case, the final mass of the black hole is $M_1 + M_2$.

For $f_{\text{seed}} = 1$ (S1) the growth is characterized by several vertical discontinuities associated with merging events, with accretion in between them playing a minor role, particularly at high redshift. Only $2.5 \times 10^5 M_\odot$, out of the final MBH mass of $1.5 \times 10^8 M_\odot$, have been accreted. For the SMBH the situation is only quantitatively different, with accretion along this branch contributing more (20%) to the growth; however, mergers are still dominating the rise of the curve.

### 3.3 Inefficient seeding scenario

In the S2 scenario $f_{\text{seed}} = 0.05$. This corresponds to a likely more physical situation in which only a minor fraction of candidate halos manage to form a IMBH seed. The best fit to the MBH – halo mass relation (Fig. [1] right panel) is $\log M_\bullet = -3.1^{+0.1}_{0.0} + 0.95^{+0.01}_{-0.0} \log M_h$, i.e., not too different from S1. The ratio $M_\bullet/M_\star$ is also very similar to S1, apart from a slightly higher variance at low BH masses. To be more quantitative, the BH mass in halos $10^{11.12} M_\odot$ is only 25 - 30% larger in S2 with respect to S1. These results are not particularly surprising as the two scenarios are bound to satisfy the same constraints.

However, the key difference is that because of the scarcer availability of seeds, the required production of SMBHs requires a higher Eddington ratio, $\lambda_E = 0.22$ in order to accrete sufficient mass. However, if we force the LBG MBH (and lower mass BH) to accrete at the Eddington ratio required by the X-ray limits, $\lambda_E = 2 \times 10^{-3}$, the early phase of the growth is strongly suppressed – also lacking a major merger contribution, and would be too slow to climb up to the SMBH range. Hence, $\lambda_E$ has to be larger even in the MBH regime. For simplicity we have then assumed a constant $\lambda_E = 0.22$ in the entire BH mass range. Clearly, with this accretion rate LBG MBHs ($M_\bullet \approx 10^8 M_\odot$) would be very luminous in X-rays. From eq. [3] we obtain $L_X = 1.0 \times 10^{44} \text{erg s}^{-1}$ (for $f_X = 0.0153$, averaged over the soft and hard X-ray bands, and for the appropriate bolometric luminosity), and hence largely exceeding the CDFs upper limit $L_X = 3 \times 10^{42} \text{erg s}^{-1}$.

We are forced to assume that the X-ray flux from BHs in LBGs (and to a much smaller, but not negligible extent also in quasars) must be locally absorbed by intervening gas and dust. The transmitted fraction of the X-ray luminosity,
$T_X$, can be determined by imposing that $T_X L_X = L_X^\star$, or $T_X = 0.03$. The required optical depth to $\approx 1$ keV photons to achieve such reduction is $\tau_X = -\ln T_X \approx 3.53$, which for a solar metallicity gas implies an absorbing column $N_H = 1.44 \times 10^{22} \text{cm}^{-2}$. We note that this conclusion perfectly agrees with LBG simulations at $z = 6$, see e.g. Fig. 2 of Behrens et al. (2019). This value is also consistent within 1$\sigma$ with those found by Trebitsch et al. (2019a) and Ni et al. (2020).

The differences between S2 and S1 are also evident in the growth history of BHs hosted by LBGs and QSOs. Looking again at Fig. 2 we see that the $f_{\text{seed}} = 0.05$ blue curves are smoother, as a result of the more continuous growth associated with accretion. Indeed, both for LBG and QSO black holes, the growth is completely (97%) dominated by accretion, with mergers playing a negligible role. This different balance between the two mechanisms entails an initial slower BH growth in S2. For example, the LBG (left panel) BH at $z \approx 8$ is about 20× less massive than predicted in S1, for which $M_* = 4 \times 10^7 M_\odot$. The same effect is visible also in the QSO BH track (right panel), albeit shifted to a higher redshift range $z = 10 - 12$. Eventually, the growth in S2 catches up with that of S1 at $z = 6$.

As the growth history encodes a memory of the initial seeding physics, it opens very interesting experimental perspectives to test when and where the first IMBH appeared on the cosmic stage. Proving the existence of an efficient seeding scenario, with relevant consequences on the production of UV photons in the early Universe.

4 MASSIVE BLACK HOLES IN LBGs

Having clarified the relation between MBHs and their host halo, to enable a meaningful observational comparison it is necessary to connect the properties of MBHs to those of the Lyman Break Galaxy population. To this aim we use available galaxy UV luminosity functions (LF) to associate a UV AB magnitude at 1375Å, $M_{\text{UV}}$, to each halo. We then compute the MBH UV luminosity from our model, and finally combine the two in the total UV LF.

4.1 Galaxy UV luminosity

Bouwens et al. (2015) have studied $\approx 10400$ star forming galaxies at redshift $4 < z < 10$, and derived their UV LF. We then adopt their data at $z = 6$, and perform an abundance matching analysis to associate a $M_{\text{UV}}$ to each halo mass. This entails solving the following equation:

$$\int_{M_h}^{+\infty} \frac{dn}{dM_h} dM_h' = \int_{-\infty}^{M_{\text{UV}}} \frac{dn}{dM_{\text{UV}}} dM_{\text{UV}}'. \quad (5)$$

In the previous expression $dn/dM_h$ is the halo mass function (Sheth et al. 2001) implemented in the numerical code developed by Murray et al. (2013); $dn/dM_{\text{UV}}$ is the experimentally determined LF at $z = 6$ (Bouwens et al. 2015).

The resulting relation between halo mass and the UV luminosity of the galaxy is reported in Fig. 3. For reference, the typical $M_h = 10^{12} M_\odot$ LBG halo hosts a galaxy with UV luminosity of $5 \times 10^4 \text{erg s}^{-1}$. Using the standard Kenicutt (1998) conversion factor of $4.46 \times 10^9 L_\odot/M_\odot \text{yr}^{-1}$, such luminosity corresponds to a star formation rate SFR = $28.7 M_\odot \text{yr}^{-1}$.
For completeness, we derive also the X-ray luminosity produced by high-mass X-ray Binaries (hereafter, XRB) and associated with this SFR. Locally (Mineo et al. 2012; Mesinger 2015) the following relations holds:

\[ L_{0,\text{XRB}} = 3 \times 10^{39} \left( \frac{\text{SFR}}{M_\odot \text{yr}^{-1}} \right) \text{erg s}^{-1}. \]  

(6)

According to Dijkstra et al. (2012) and Lehner et al. (2016) the local relation evolves up to \( z = 7 \) as follows:

\[ L_{\text{XRB}}(z) \approx L_{0,\text{XRB}}(1 + z); \]  

(7)

we refer to Orofino et al. (2018) for more details. At \( z = 6 \) this yields \( L_{\text{XRB}} = 6 \times 10^{40} \text{erg s}^{-1} \). Hence, the XRB luminosity is \( \approx 0.2L_X^\star \). Note, in addition, that HMXB have a much softer spectrum with respect to AGN, and therefore most of their restframe luminosity is redshifted out of the Chandra bands. For these reasons, we conclude that at best the HMXB impact on our results is small.

### 4.2 BH UV luminosity

From the results obtained in Sec. 3 it is straightforward to compute the UV BH luminosity, using the derived \( M_\bullet \) and \( \lambda_E \) values for the two scenarios, along with eq. [3] and the bolometric correction by Shen et al. (2020); this is displayed in Fig. 3. However, due to obscuration effects, the calculation for S2 requires an extra step.

We have seen that in a typical LBG, X-ray emission must be absorbed by a gas column \( N_H = 1.44 \times 10^{22} \text{cm}^{-2} \). The corresponding optical depth at 1450Å, adopting a Milky Way \( R_V = 3.1 \) extinction curve (Weingartner & Draine 2001) and solar metallicity, is \( \tau_{\text{UV}} = \text{\sigma}_{\text{UV}}N_H = 4.8 \times 10^{-22} \text{AN}_H = 19.4 \), where \( A = 2.75 \) is the 1450Å-to-V band attenuation ratio (Ferrara et al. 2019). Differently from X-rays, whose opacity is dominated by gas photoelectric effects, (non-ionizing) UV photons mostly interact with dust by which they are absorbed and scattered. In spite of the large UV optical depth, scattering enables a varying fraction, \( T_{\text{UV}} \), of photons to escape from the system. \( T_{\text{UV}} \) depends on \( \tau_{\text{UV}} \), and on the optical properties of dust grains, namely the albedo \( \omega \), and the Henyey-Greenstein scattering phase function \( g \). The classical solution (Code 1973) for a central source surrounded by a spherical gas/dust distribution obtained with the two-stream approximation, and confirmed by Monte Carlo radiative transfer simulations (Ferrara et al. 1999), is appropriate here. This yields the transmitted UV fraction

\[ T_{\text{UV}} = \frac{2}{(1 + \zeta)e^{\xi_{\text{UV}}} + (1 - \zeta)e^{-\xi_{\text{UV}}}}, \]  

(8)

where

\[ \zeta = \sqrt{(1 - \omega)}/(1 - \omega g) = 0.916, \]  

(9)

and

\[ \xi = \sqrt{(1 - \omega)/(1 - \omega g)} = 0.691, \]  

(10)

having assumed the appropriate MW dust parameters \( \omega = 0.3668 \) and \( g = 0.6719 \) (Weingartner & Draine 2001). We then find \( T_{\text{UV}} = 2 \times 10^{-6} \) for a MBH hosted by a LBG halo. Such value is much larger than that for a pure absorption case \( 5.4 \times 10^{-5} \), obtained by setting the albedo \( \omega = 0 \) in eq. [8]. However, the gas is well known to be clumpy in the circumnuclear regions of AGN (Bianchi et al. 2000; specifically see their Fig. 1) showed that this situation leads to a lower effective \( \tau_{\text{UV}} \). They find that for a realistic case in which 75% of the gas mass is in clumps (clumping factor \( f_c = 0.75 \)) the effective optical depth is \( \tau_{\text{UV}} \approx 3.5 = 5.55 \). Then, the corresponding (effective) transmissivity is \( T_{\text{UV}} = 0.023; \)

12 Online digital data for the adopted configuration can be found at www.arcetri.astro.it/~sbianchi/attenuation/E_MC.att
note that, by chance, $T_{UV} \approx T_X$. As a guide we will then assume this value when discussing S2 implications for LBGs in S1.

Similarly, $T_{UV}$ for QSO is derived by imposing that the bolometric luminosity in our most massive halo is $10^{47}$ erg s$^{-1}$; we linearly interpolate values of $T_{UV}$ from the QSO to the LBG halo ranges, and keep it constant below the LBG halo mass. Finally, the emerging UV luminosity, as a function of the BH mass, is

$$L_{UV}^\star = T_{UV}^\star f_{UV} \lambda_E L_E.$$  \hspace{1cm} (11)

For the LBG, the predicted BH UV luminosity in S1 (S2) is $L_{UV}^\star = 1.5 (3) \times 10^{40}$ erg s$^{-1}$. The BH contribution to the total (galaxy + BH) luminosity increases with halo mass (the relative ratio of the two components is displayed in the bottom panel of the Fig. [3]).

In the LBG halo mass range $10^{11}$–$10^{12} M_\odot$, the BH luminosity is $\simeq 1/50$ of the stellar one. However, this ratio raises in more massive halos until the BH outshines the host galaxy by a factor $\simeq 3$–4 in quasars. These results are qualitatively the same for both scenarios. BHs in S2 are $\approx 5$ times more luminous compared to S1 in the LBG range. This is mostly due to the different value of the product $T_{UV}^\star \lambda_E$.

For QSOs, S1 and S2 yield the same results, because they are both anchored to the QSO abundance constraints. We recall that as in S2 $\lambda_E$ is about 100× higher in the LBG regime, the CDF's X-ray and QSO constraints can only be satisfied if the BH emission in LBGs is heavily absorbed (see Sec. 5.3). The previous results suggest that UV luminosity of LBG is largely dominated by stars. Although we are not dealing with ionizing photons, this finding resonates with those by Trebitsch et al. (2020) who conclude that faint AGN do not contribute significantly to cosmic reionization.

4.3 UV luminosity function

We are now ready to predict the BH contribution to the observed galaxy UV LF. This can be formally written as

$$\phi \equiv \frac{dn}{dL_{UV}} = \frac{dn}{dm_{BH}} \frac{dm_{BH}}{dM_{BH}} \frac{dM_{BH}}{dM_{UV}},$$ \hspace{1cm} (12)

where $dm_{BH}/dM_{BH}$ and $dM_{BH}/dL_{UV}$ are the BH-halo mass relation, and the BH mass dependence of the UV luminosity, respectively. Fig. 4 shows the results of this calculation for S1 and S2, after a final conversion of the UV luminosity into an absolute AB magnitude, $M_{UV}$, at 1375 Å.

In both scenarios the LF is largely dominated by stellar emission up to very bright magnitudes $M_{UV} \simeq -23$. At luminosities fainter than this, the BH LF has a power law shape extending to $M_{UV} \simeq -17.5$; at even fainter fluxes the BH LF becomes uncertain as the Eddington ratio is not constrained. The fraction of galaxies powered by a BH at $M_{UV} \simeq -17.5$ is $10^{-3}$; this ratio increases to $6 \times 10^{-3} (1.0)$ at $M_{UV} \simeq -22 (-23.5)$. The very bright end of the LF is dominated by rare ($\phi < 10^{-6}$) sources in which BH emission outshines star formation (i.e. quasars). There, the LF deviates from the Schechter function and becomes a power-law.

These results agree well with available data from large survey such as the SHELLQ (Matsuoka et al. 2018), GOLDRUSH (Ono et al. 2018), and SHEL (Stevans et al. 2018). SHELLQ, in particular, measured the quasar UV LF at $z \approx 6$ over the wide mag range $-30 < M_{UV} < -22$. The observed ratio of galaxies powered by a BH at $M_{UV} \simeq -22 (-23.5)$ is $1.6 \times 10^{-3}(1)$, in almost perfect agreement with our results (note that the measurement at the faintest $M_{UV} < -22$ luminosity is affected by a considerable error). While the normalization of the LF at $M_{UV} = -23.5$ also agrees with SHELLQ (note that the BH and galaxy LFs overlap at this magnitude), predicting a BH density of $10^{-8}$ Mpc$^{-3}$, the faint-end slope $\alpha$ of our black hole LF function is steeper. We find $\alpha = -2.5$, which must be compared with the SHELLQ best fit value $\alpha = -1.25^{+0.44}_{-0.34}$. We note that our faint-end slope is marginally consistent with that derived by Onoue et al. (2017), $\alpha = -2.04^{+0.15}_{-0.13}$, who included also X-ray detected AGN from Parsa et al. (2018), and the multi-redshift determination by Manti et al. (2017), $\alpha = -1.33^{+0.13}_{-0.08}$. This discrepancy likely indicates that a considerable fraction of AGN at $z = 6$ is indeed obscured as we confirm here. Interestingly the two seeding scenarios cannot be disentangled purely from the LF. This is because they are both bound to satisfy the observational constrains at the LBG and QSO mass scales. However, we recall that in order to satisfy those constrains – in S2 a large fraction of the accretion luminosity must be absorbed by gas and dust. This has important implications that we discuss in the next Section.

5 IMPLICATIONS AND TESTS

The previous analysis suggests that the assumption that LBGs host MBH is consistent with observational constraints. In order to circumvent the tight limits imposed by X-ray observations, one has to assume that either such MBHs accrete at a very low rate (scenario S1), or their emission is obscured (S2). Although neither possibility can be discarded, we recall that S1 requires a, perhaps implausible, maximal efficiency of seed formation via the direct collapse mechanism. For this reason, we concentrate next on the implications of S2, and the possible ways to test them.

5.1 Infrared emission

We have seen that in a typical LBG, $\tau_{UV}^\star = 5.5$, implying that $>99.6\%$ of the UV luminosity produced by the MBH, $L_{UV}^\star (1 - T_{UV}^\star)/T_{UV}^\star \simeq f_{UV} \lambda_E L_E$, is absorbed by dust, and converted into thermal infrared emission. We recall from Sec. 5.3 that $\lambda_E = 0.22$, $M_{BH} = 10^7$ $M_\odot$, and $L_E = 3 \times 10^{46}$ erg s$^{-1}$, hence, the unobserved, intrinsic UV luminosity is $1.31 \times 10^{48}$ erg s$^{-1} \simeq L_{FIR}$, where $L_{FIR}$ is the total far infrared luminosity in the $8 - 1000\mu$m range. To proceed further, we need to estimate the dust mass from the absorbing column $N_H = 1.44 \times 10^{22}$ cm$^{-2}$.

We envisage two possibilities: (a) absorption is produced by a central obscurer local to the MBH, which we can tentatively identify with the dust torus, whose size we

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13 We follow Matsuoka et al. (2018), and define the slope from the power-law fit $\log(\phi/\phi^*) = -0.4(\alpha + 1)(M_{UV} - M_{UV}^\star)$.

14 We have verified that the above predicted LBG luminosities are in perfect agreement with the observed $L_X - L_{FIR}$ relation presented in Fig. 12 of Pouliasis et al. (2020).
assumed to be $R_H \approx 1$ pc (Netzer 2015); (b) the absorbing dust is part of the interstellar medium of the host LBG (Circosta et al. 2019). Numerical simulations (Barai et al. 2018) indicate that $N_H \approx 10^{22} \text{cm}^{-2}$ is found at a typical distance $R_H \approx 500$ pc from the center in AGN-host galaxies with a halo mass of $\approx 10^{12} M_{\odot}$. The dust mass (assuming a dust-to-gas ratio $D = 1/162$ (Galliano et al. 2008)) is then $M_d = (2.87 \times 10^5) M_{\odot}$ for (a) and (b), respectively.

The dust temperature, $T_d$, is determined by the following expression (Hirashita et al. 2014), which assumes a gray-body emission:

$$T_d = \left( \frac{f_{\nu} \lambda_{\nu} k_{\nu} L_{\nu}}{\Theta M_d} \right)^{1/(4+\beta)}; \quad (13)$$

where

$$\Theta = \frac{8 \pi \kappa_{158} \kappa_{B}^{4+\beta} B_{158}^{4+\beta} \zeta (4+\beta) \Gamma (4+\beta)}{c^2 \rho_{158} \lambda_{158}^{4+\beta}} = 1.02 \times 10^{-5}, \quad (14)$$

the mass absorption coefficient, $\kappa_{\nu} = \kappa_{158} (\nu/\nu_{158})^{\beta}$ is pivoted at the reference wavelength of $158 \mu m$ since high-$z$ ALMA observations are often tuned to the rest wavelength of [CII] emission. We take $\kappa_{158} = 20.9 \text{cm}^2 \text{g}^{-1}$, $\beta = 2$ appropriate for graphite grains following (Dayal et al. 2010) and references therein; $\zeta$ and $\Gamma$ are the Zeta and Gamma functions, respectively; the other symbols have the usual meaning. We then obtain $T_d = (533, 78)$ K for (a) and (b), respectively. As expected, dust located close to the MBH gets hotter. The peak temperature for the gray-body adopted here is $T_{\nu} = 0.29/T_d$, hence yielding $T_{\nu} = (5.4, 43.1) \mu m$. For a LBG located at $z \approx 6$, the redshifted emission peak nicely falls in the SW/SMI bands of SPICA for case (a); for case (b) the Rayleigh-Jeans portion of the spectrum is at reach of ALMA. It is then useful to compute the expected flux in these two cases. By applying the standard formula

$$f_{\nu} = \frac{(1+z) \kappa_{(1+z)\nu} M_d B_{(1+z)\nu} (T_d)}{a_{158}^2} \quad (15)$$

we predict a flux of $(38, 27) \mu Jy$ in the SPICA SW/SMI band and for ALMA Band 6; these fluxes are well at reach of these instruments. While SPICA is still in the planning phase, available ALMA continuum observations of $z \approx 5 - 6$ LBGs at 158 $\mu m$ indeed report fluxes that are comparable to the above one. For example, Hz6 a LBG at $z = 5.3$ part of the Capak et al. (2015) sample with $M_{UV} = -22.5$, hence comparable to the reference LBG considered here, has a measured continuum flux of $129 \pm 36 \mu Jy$. Hence, according to our results, $>16\%$ of the observed flux could be contributed by MBH accretion luminosity if the obscuring dust is located in the Narrow Line Region.

In summary, hot dust is expected only if a MBH is present and the dust obscurer is local ($\approx 1$ pc) to it; if absorption occurs on larger scales (comparable to the NLR, several hundreds pc) stars and MBH accretion contribute similarly to observed continuum flux. Hence, a MBH cannot be excluded by a SPICA non-detection; an ALMA detection cannot uniquely disentangle the MBH contribution from the stellar one.

5.2 UV emission lines

To make progress, it is necessary to combine FIR probes with an unique feature of MBH accretion, such as UV emission lines. In particular, we should search for ionized species with an ionization potential $>4$ Ryd, which cannot be produced by even the hardest (e.g. binaries) stellar radiation sources, with the possible exception of elusive Pop III stars for HeII (Pallottini et al. 2015). The most suitable candidates are then the $\lambda \nu 1240$ (IP$=77.47$ eV) and HeII $1640$A (IP$=54.4$ eV) lines. Laporte et al. (2017) recently re-
ported a $\approx 5\sigma$ detection of these two lines in the redshift $z = 7.15$ galaxy COSY ($M_{\text{UV}} = -21.8$, SFR $= 20.2 \, M_{\odot} \, \text{yr}^{-1}$), opening the interesting possibility that this system might host a central MBH powering them. The measured rest-frame equivalent widths (EWs) is $3.2_{-0.8}^{+4.8} \, \AA$ and $2.5_{-1.3}^{+1.3} \, \AA$ for Nv and HeII, respectively. COSY is undetected in the $158 \, \mu\text{m}$ continuum (upper limit $< 14 \, \mu\text{Jy}$), which, according to eq. (16) should imply a AGN-heated dust with temperature $T_d \lesssim 90 \, \text{K}$, and distributed within $300 \, \text{pc}$ of the MBH.

Dietrich et al. (2002) studied 744 Type 1 AGN in $0 < z < 5$, spanning nearly 6 orders of magnitude in continuum. They find that, almost independently of redshift, the EWs of most emission lines (including HeII) significantly anti-correlate with the continuum strength (akin to the “Baldwin effect”); the NV EW is instead almost independent of $L_{\text{UV}}$. For our predicted observed luminosity of $3.1 \times 10^{45} L_{\text{UV}} = 3 \times 10^{45} \, \text{erg s}^{-1}$, their relations (Fig. 7 of their paper) indicate a EW of $30 \, \AA$ and $20 \, \AA$ for Nv and HeII, respectively. Given that our MBH is significantly obscured, we need to correct these EWs for line absorption. A simple correction can be obtained by using the line escape probability, $\beta$, as a function of the medium optical depth (as both lines are in the UV, we assume the same optical depth, $\tau_{\text{UV}} = 5.5$, derived in Sec. 4). Such formalism (see e.g. Netzer (1990)) states that the probability for a line to escape from the system is

$$\beta \simeq \frac{1}{1 + 2\tau_{\text{UV}}} = 0.083.$$

After correcting for this effect the two EW become equal to $\simeq 2.49 \, \AA$, for Nv and $\simeq 1.66 \, \AA$, for HeII in qualitative agreement (barred the many uncertainties) with the observed values, including their relative ratio. Although this simplistic treatment cannot represent a conclusive argument, it clearly points towards the possibility that indeed COSY hosts a MBH with properties similar to those predicted here.

5.3 Outflows

Accreting black holes might launch powerful outflows by converting their radiative energy into kinetic one. In a dusty medium, radiation pressure does not rely purely on Thomson scattering on electrons but it can additionally transfer momentum via an efficient coupling with dust grains. The amplification (or “boost”) factor of the radiation force in the UV bands is $A = \sigma_{\text{UV}}/\sigma_T \approx 1900$, where $\sigma_T$ is the Thomson cross-section, thus favoring the onset of radiation-pressure driven outflow from the galaxy. A proper treatment must include the frequency-weighting over the AGN spectrum. The calculation has been performed by Fabian et al. (2008) as a function of the absorbing gas column density. In their model, they show that the boost factor is the inverse of the Eddington factor, $A = \lambda_0^{-1}$.

Fig. 5 shows $\lambda_0$ vs. $N_H$ for a high-$\lambda_0$ AGN spectrum. Systems lying in the low $N_H$ – high $\lambda_0$ region to the left of the curve develop powerful outflows, particularly if $N_H > 21.7 \, \text{cm}^{-2}$, this is consistent also with Ni et al. (2020).

Lower columns provide only a weak coupling to the radiation, leading only to the possible formation of filamentary structures (“dust lanes”). The predicted location of the typical, $M_{\text{UV}} = -22$, LBG galaxy at $z = 6$ (blue point in Fig. 5) falls in the region in which outflows should develop. We recall that the $N_H$ derived from the CDFs X-ray data represents a lower limit, as indicated by the arrow. If the ISM is clumpy, as assumed in Sec. 4.2, the column density in the $x$-axis of Fig. 5 must be interpreted as referring to the clumps, which will therefore be individually accelerated. For a dedicated numerical work see, e.g. Roth et al. (2012).

Evidences for outflows in high-$z$ LBGs are rapidly accumulating, particularly thanks to the availability of ALMA observations. The original claim by Gallerani et al. (2018) from a stacking analysis of the Capak et al. (2015) sample, has been now confirmed by the ALPINE Large Program (Galloni et al. 2020; Fudamoto et al. 2020). Fast outflows have been tentatively identified in $z = 5–6$ galaxies also by using deep Keck metal absorption line spectra (Sugahara et al. 2019).

Obviously, it might well be that these outflows are driven by supernova energy, rather than by a hidden AGN. Pizzati et al. (2020) showed that stellar outflows might explain the extended (size $\approx 10 \, \text{kpc}$) [CII] halos observed around LBGs at $z = 4–6$ (Fujimoto et al. 2019; 2020). Interestingly, though, these authors noted that the required relatively large outflow loading factor, $\eta = 3.2$, is only marginally consistent with starburst-driven outflows, and might instead indicate an additional energy input from a hidden AGN. Investigating the nature of outflows energy sources might lead to considerable progress in understand-
6 SUMMARY

To address the possible presence of faint AGN powered by MBH in Lyman Break Galaxies in the Epoch of Reionization, we have run merger tree simulations implanted with direct collapse black hole seeds of mass $10^5 M_\odot$, according to the prescriptions given in [Ferrara et al. 2014]. The BH growth, which can occur via BH-BH merging and matter accretion, is followed down to $z = 6$ with an accretion rate determined by the Eddington ratio, $\lambda_E$, whose values is constrained by X-ray LBG and SMBH abundance/luminosity data. Depending on the seeded halo fraction, $f_{\text{seed}}$, corresponding to different feedback-regulated formation efficiencies of direct collapse BHs, we consider (a) maximal seeding ($f_{\text{seed}} = 1$, S1), and (b) inefficient seeding ($f_{\text{seed}} = 0.05$, S2) scenarios.

The two scenarios predict a very similar $M_*/M_h \simeq 2 \times 10^{-4}$ relation at $z = 6$. This is not surprising as they are bound to satisfy the same observational constraints. However, they widely differ in many other properties. For example, in a typical LBG galaxy ($M_h = 10^{12} M_\odot$, $M_{\text{UV}} = -22$, $n = 10^{-5} \text{Mpc}^{-3}$) accreted matter represents only 5\% of the final MBH mass, the rest being acquired by merging. Instead, in S2 accretion dominates in the (super-)massive BH range. It follows that, to satisfy X-ray constraints, the MBH luminosity in S2 must be obscured by an absorbing gas column density $N_H = 1.44 \times 10^{22} \text{cm}^{-2}$, corresponding to a soft X-ray optical depth $\tau_X > 3.51$ (transmissivity $T_X < 0.03$). For the QSO absorption is instead very small. In addition, S2 predicts an initial slower BH growth: proving the existence of direct collapse BHs, we consider (a) maximal seeding ($f_{\text{seed}} = 1$, S1), and (b) inefficient seeding ($f_{\text{seed}} = 0.05$, S2) scenarios.

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We predict that the observed UV LF in both scenarios is largely dominated by stellar emission up to very bright mag, $M_{\text{UV}} \simeq -23$, with BH emission playing a subdominant role. This finding is in agreement with the results by [Volonteri et al. 2017]. The fraction of galaxies powered by a BH at $M_{\text{UV}} \simeq -17.5$ is $10^{-3}$; this ratio increases to $6 \times 10^{-3}$ (1\%) at $M_{\text{UV}} \simeq -22$ ($\sim 2.5$). It is interesting to compare these predictions with available data for luminous LBGs, [Capak et al. 2015] carried out ALMA [Cii] observations of 10 LBGs at $z = 5 - 6$; these sources have UV magnitudes in the range $-22.8 < M_{\text{UV}} < -21.5$. Among these, only 1 (H25) is classified as an AGN. We predict that the expected frequency of AGN in Capak’s sample should have been $0.1\% \pm 0.02$, in outstanding agreement with the 0.1 value found. Our results also are generally consistent with available QSO LF determinations, but the predicted faint-end slope $\alpha \simeq -2.2$ is steeper than that derived by SHELLQ [Matsuoka et al. 2018].

Although the two scenarios are both viable, S1 postulates a 100\% efficiency of seed formation. As such, for the more realistic S2 scenario in which MBHs grow by obscured accretion, we have explored the following implications:

□ Infrared emission If the obscurer is local ($z \simeq 1$ pc) to the MBH, the amount of dust implied is very small, $2.8 M_\odot$;

□ Emission lines Although ALMA FIR continuum observations alone cannot conclusively pinpoint the presence of a faint AGN in LBGs, they can be combined with UV emission lines such as Nv and Heii uniquely tracing AGN hard radiation. We show that the detected EWs of these two lines in COSY, a LBG galaxy at $z = 7.15$ are successfully reproduced by our model, thus supporting the suggestion that COSY hosts an obscured MBH with properties similar to those predicted here.

□ Outflows A MBH in a typical LBG galaxy, with the $\lambda_E$ and $N_H$ predicted here, should launch a powerful outflow according to the model by [Fabian et al. 2008]. This prediction is preliminarily supported by a number of recent findings, including the ALMA ALPINE survey, highlighting the presence of outflows that are only marginally consistent with starburst energetics, and might therefore require an additional energy contribution from a hidden, faint AGN.

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REFERENCES

Agarwal B., Khochfar S., 2015, MNRAS, 446, 160
Agarwal B., Smith B., Glover S., Natarajan P., Khochfar S., 2016, MNRAS, 459, 4209
Alvarez M. A., Wise J. H., Abel T., 2009, ApJ, 701, L133
Armitage P. J., Natarajan P., 2005, ApJ, 634, 921
Atek H., Richard J., Kneib J.-P., Jauzac M., Schaerer D., Clement B., Limousin M.,Jullo E., Natarajan P., Egan E., Ebeling H., 2015, ApJ, 800, 18
Aversa R., Lapi A., de Zotti G., Shankar F., Danese L., 2015, ApJ, 810, 74
Barai P., Gallerani S., Pallottini A., Ferrara A., Marconi A., Ci-ccone C., Maiolino R., Carniani S., 2018, MNRAS, 473, 4003
Begelman M. C., Rees M. J., 1978, MNRAS, 185, 847
Behrens C., Pallottini A., Ferrara A., Gallerani S., Vallini L., 2019, MNRAS, 486, 2197
Behroozi P., Wechsler R. H., Hearin A. P., Conroy C., 2019, MNRAS, 488, 3143
Bianchi S., Ferrara A., Davies J. I., Alton P. B., 2000, MNRAS, 311, 601
Boco L., Lapi A., Danese L., 2020, ApJ, 891, 94
Bortolas E., Capelo P. R., Zana T., Mayer L., Bonetti M., Dotti M., Davies M. B., Madau P., 2020, arXiv e-prints, p. arXiv:2005.02409
Parsa S., Dunlop J. S., McLure R. J., 2018a, MNRAS, 474, 2904
Parkinson H., Cole S., Helly J., 2008, MNRAS, 383, 557
Parsons B., Dunlop J. S., McLure R. J., 2018a, MNRAS, 474, 2904
Park K., 2012, PhD thesis, University of Maryland, College Park
Park K., Ricotti M., 2013, ApJ, 767, 163
Parkinson H., Cole S., Helly J., 2008, MNRAS, 383, 557
Parsi A., Dunlop J. S., McLure R. J., 2018b, MNRAS, 474, 2904

Pensabene A., Carniani S., Perna M., Cresci G., Decarli R., Maiolino R., Marconi A., 2020, arXiv e-prints, p. arXiv:2002.00958
Petri A., Ferrara A., Salvaterra R., 2012, MNRAS, 422, 1690
Pfister H., Volonteri M., Dubois Y., Dotti M., Colpi M., 2019, MNRAS, 486, 101
Pizzati E., Ferrara A., Pallottini A., Gallerani S., Vallini L., Decataldo D., Fujimoto S., 2020, arXiv e-prints, p. arXiv:2001.10547
Planck Collaboration Aghanim N., ... 2018, arXiv e-prints, p. arXiv:1807.06209
Pouliasis E., Mountrichas G., Georgantopoulos I., Ruiz A., Yang M., Bonanos A. Z., 2020, Monthly Notices of the Royal Astronomical Society
Quinlan G. D., Shapiro S. L., 1990, ApJ, 356, 483
Rees M. J., 1984,ARA&A, 22, 471
Regan J. A., Downes T. P., Volonteri M., Beckmann R., Lupi A., Trebitsch M., Dubois Y., 2019, MNRAS, 486, 3892
Reines A. E., Volonteri M., 2016, in American Astronomical Society Meeting Abstracts #227 Vol. 227 of American Astronomical Society Meeting Abstracts, Relations Between Black Hole Mass and Total Galaxy Stellar Mass in the Local Universe. p. 119.01
Roth N., Kasen D., Hopkins P. F., Quataert E., 2012, The Astrophysical Journal, 759, 36
Salvati M., Volonteri M., Gehrels N., Bonning E. W., 2007, ApJ, 662, 131
Schmittfull J. D., Buonanno A., 2007, ApJ, 662, L63
Shankar F., Weinberg D. H., Shen Y., 2010, MNRAS, 406, 1959
Shapiro S. L., Teukolsky S. A., Lightman A. P., 1983, Physics Today, 36, 89
Shen X., Hopkins P. F., Quintero M., Alexander D. M., Richards G. T., Ross N. P., Hickox R. C., 2020, arXiv e-prints, p. arXiv:2001.02696
Sheth R. K., Mo H. J., 2001, MNRAS, 323, 1
Spitzer Jr. L., 1969, ApJ, 158, L139
Stark D. P., Wirth G., Naiman D., Bertone E., Gutkin J., Richard J., Mainali R., Robertson B., Siana B., Tang M., Schmittfull J. D., 2015, MNRAS, 454, 1393
Stevans M. L., Finkelstein S. L., Wolf I., Kawinwanichakij L., Papovich C., Shuerman S., Ciardullo R., Florez J., Gronwall C., Jogee S., Somerville R. S., Yung L. Y. A., 2018, ApJ, 863, 63
Sugarahara Y., Ouchi M., Harikane Y., Bouché N., Mitchell P. D., Blaizot J., 2019, ApJ, 886, 29
Sugimura K., Onoue M., Inoue A. K., 2014, MNRAS, 445, 544
Sugimura K., Ricotti M., 2020, arXiv e-prints, p. arXiv:2003.05625
Suh H., Civano F., Hasinger G., Lusso E., Marchesi S., Schulze A., Onodera M., Rosario D. J., Sanders D. B., 2019, ApJ, 872, 168
Takeo E., Inayoshi K., Mineshige S., 2020, arXiv e-prints, p. arXiv:2002.07187
Tamburello V., Capelo P. R., Wadsley J., 2015, ApJ, 810, 51
Tamburello V., Capelo P. R., Mayer L., Bellovary J. M., Wadsley J., 2015, ApJ, 810, 51
Liu T., Paolillo M., Ranalli P., Schneider D. P., Shemmer O., Volonteri M., Wang J., 2018, MNRAS, 473, 2378
Volonteri M., Dubois Y., Pichon C., Devriendt J., 2016, MNRAS, 460, 2979
Volonteri M., Rees M. J., 2006, ApJ, 650, 669
Volonteri M., Reines A. E., Atek H., Stark D. P., Trebitsch M., 2017a, ApJ, 849, 155
Volonteri M., Reines A. E., Atek H., Stark D. P., Trebitsch M., 2017b, ApJ, 849, 155
Volonteri M., Silk J., Dubus G., 2015, ApJ, 804, 148
Wang R., Carilli C. L., Neri R., Riechers D. A., Wagg J., Walter F., Bertoldi F., Menten K. M., Omont A., Cox P., Fan X., 2010, ApJ, 714, 699
Weingartner J. C., Draine B. T., 2001, ApJ, 548, 296
Willott C. J., Bergeron J., Omont A., 2015, ApJ, 801, 123
Willott C. J., Delorme P., Omont A., Bergeron J., Delfosse X., Forveille T., Albert L., Reylé C., Hill G. J., Gully-Santiago M., Vinten P., Crampton D., Hutchings J. B., Schade D., Simard L., Sawicki M., Beelen A., Cox P., 2007, AJ, 134, 2435
Yue B., Ferrara A., Salvaterra R., Xu Y., Chen X., 2014, MNRAS, 440, 1263