Geometry and optics calibration of WFCTA prototype telescopes using star light

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Abstract The Large High Altitude Air Shower Observatory project is proposed to study high energy gamma ray astronomy (40 GeV-1 PeV) and cosmic ray physics (20 TeV-1 EeV). The wide field of view Cherenkov telescope array, as a component of the LHAASO project, will be used to study energy spectrum and compositions of cosmic ray by measuring the total Cherenkov light generated by air showers and shower maximum depth. Two prototype telescopes have been in operation since 2008. The pointing accuracy of each telescope is crucial to the direction reconstruction of the primary particles. On the other hand the primary energy reconstruction relies on the shape of the Cherenkov image on the camera and the unrecorded photons due to the imperfect connections between photomultiplier tubes. UV bright stars are used as point-like objects to calibrate the pointing and to study the optical properties of the camera, the spot size and the fractions of unrecorded photons in the insensitive areas of the camera.

Key words Cosmic ray, Cherenkov telescope, Calibration

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1 Introduction

The Large High Altitude Air Shower Observatory (LHAASO)\textsuperscript{1]} project aims to study high energy gamma ray astronomy (40 GeV-1 PeV) and cosmic ray physics (20 TeV-1 EeV). The Wide Field of View (FOV) Cherenkov telescope Array (WFCTA), as a component of the LHAASO project, is designed to study cosmic ray energy spectrum specie by specie by measuring the energy and $X_{\text{max}}$ depth of each air shower.

Two WFCTA prototype telescopes have been constructed and placed nearby the ARGO-YBJ experimental hall. The two telescopes can be operated in both monocular and stereo modes, while coincident observation with the ARGO-YBJ detector is achieved off-line.

Each telescope is made up of two main parts, the reflector and the camera. The reflector consists of 20 spherical mirrors with a radius curvature $R$ of 4740±20 mm, corresponding to a total area of 4.7 m$^2$. The reflecting efficiency of the mirrors is about 82% for light with wavelength larger than 300 nm. A camera is placed at the focal plane which is 2305 mm away from the reflector center to optimize the spot shape of a point-like object. The camera is composed of 256 flat hexagonal photomultipliers tubes (PMTs) each of which has a diameter of 40 mm, corresponding to a FOV of about $1^\circ \times 1^\circ$. The PMTs are arranged in 16 columns and 16 rows forming a total FOV of $14^\circ \times 16^\circ$\textsuperscript{2]}. The maximum quantum efficiency of PMTs can reach 30% at 420 nm\textsuperscript{3]. The signals of the PMTs are digitized by 50 MHz Flash Analog to Digital Converters (FADCs). The whole system is hosted in a shipping container with a dimension of 2.5 m×2.3 m×3 m. The container is mounted on a standard dump-truck frame with a hydraulic lift that

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allows the container to be tilted in any elevation angles from 0 to 60 degrees. The pointing direction of the telescope can be easily changed [2].

The pointing accuracy and geometry properties of the telescopes are crucial to the arrival direction and $X_{\text{max}}$ reconstructions. The energy reconstruction relies on the recorded Cherenkov image, however, due to the imperfect physical junction between PMTs, some Cherenkov photons are unrecorded in the joints. In order to improve the accuracy of energy reconstruction the optical properties are studied.

In this paper, we describe a method to calibrate the geometry and optical properties by using UV bright stars. While monitoring the UV Cherenkov light from air showers, the telescopes are also sensitive to the UV light from stars crossing the FOV of the telescopes. With their well known positions, orders of magnitude more accurate than the required resolution of WFCTA, and their point-like shape, the stars are ideal tools to test the pointing direction of each telescope. Using stars the optical properties of the telescope are studied.

2 Night sky background and star signal

In addition to record the Cherenkov light from air showers, the camera also records the night sky background light (NSB). When a bright star enters the FOV of the telescope, light from the star is added to the diffused NSB. The changes of the recorded NSB reflect the light sources crossing the FOV of the PMTs and the weather conditions. A star stays about 4 minutes in the FOV of a PMT, during this time light from the star is added to the diffused NSB. While NSB change due to weather change behaves differently, which usually lasts much longer than 4 minutes and almost all PMTs are affected at the same time. This enables star signals to be discriminated from weather change.

For each air shower event, the signal of Cherenkov light only lasts a few nanoseconds, while the trigger window lasts 18 $\mu$s, so telescopes record NSB in most of the trigger window. In order to reduce the fluctuation the recorded NSB is averaged in every 10s. Fig. 1 shows a typical NSB curve in one night recorded by a PMT. After subtracting the diffused background, peaks due to stars are clearly seen. The peak amplitude of a star light curve in a PMT depends on its UV brightness and its projected position to the PMT on the camera. In a typical night, many stars can be seen by each PMT.

3 Pointing direction

Stars with well known positions and brightness are used as guiders of the telescopes. In our analysis, the TD 1 catalog is used, which has four different wavelength bands, 1565, 1965, 2365 and 2740 Å respectively [4]. Since the WFCTA telescopes are sensitive in the near UV band, stars with flux in the 2740 Å band above $1 \times 10^{-11}$ erg/cm$^2$/s are used.

The pointing direction of each telescope can be changed through the container which encloses the whole telescope system. Only very rough pointing direction (about 200° in azimuth and 60° in elevation) is known through it. Using the rough pointing direction, the time when the brightest star appears in the FOV of the telescope can be found through the brightest PMT. However, due to the large size of the PMT, the position of the star cannot show accurately the position of the brightest star on the camera. So the weighted center position $(x_0, y_0)$ of the PMT and its neighbors within 2° is considered as the position of the star on the camera. When the star is in the middle of the camera in the horizontal direction, the star has the same azimuth angle with the telescope, while the elevation angle of the star is equal to the elevation of telescope plus the distance between the position of the star and the center of the camera. The obtained pointing direction of the telescope is more accurate than the one from the container.

After getting the pointing direction of the telescope through the brightest star, orphan stars which have no surrounding stars within 2° are used to correct the pointing direction of the telescope by using
The accuracy of the pointing direction can be described by differences between positions of stars in the local coordinates and the obtained ones. Fig. 2 shows the distribution of the differences for one telescope. An accuracy better than 0.05° is obtained in less than 20 minutes with five stars in the FOV.

4 Camera geometry

The camera geometry calibration is done after pointing correction of each telescope. The calibration includes the following four parameters. The first one \( P_1 \) is a scaling of the tubes away from the center of the tube cluster. To first order \( P_1 \) corrects for deviations in the radius curvature of a mirror and for changes in the effective camera-mirror distance due to the treatment of the flat camera as a curved surface. The second parameter \( P_2 \) describes the rotation angle of the camera around the mirror axis. The last two parameters \( P_3, P_4 \) indicate the offsets of the shift in the position of the entire camera with respect to the mirror axis. After the four parameters corrections the positions \( (x_{c,t}, y_{c,t}) \) of stars on the camera at time \( t \) are modified by Eq. (1) and Eq. (2).

\[
x'_{c,t} = (1+p_1)(x_{c,t} \cos(p_2) - y_{c,t} \sin(p_2)) + p3 \\
y'_{c,t} = (1+p_1)(x_{c,t} \sin(p_2) + y_{c,t} \cos(p_2)) + p4
\]
four parameters can be obtained by the least squared method. The \( \chi^2 \) is shown in Eq. (3).

\[
\chi^2 = \sum_{\text{star}} \sum_t \frac{(x'_{\text{star}, t} - x_{\text{star}, t})^2 + (y'_{\text{star}, t} - y_{\text{star}, t})^2}{\sigma_x^2 + \sigma_y^2}
\]

In Eq. (3), the \( x_{\text{star}, t}, y_{\text{star}, t} \) are the stars’ exact positions on the camera at time \( t \). The \( \sigma_x \) and \( \sigma_y \) are the RMS of the \( x'_{\text{star}, t} \) and \( y'_{\text{star}, t} \), respectively. By minimizing the \( \chi^2 \), the values of \( P_1, P_2, P_3 \) and \( P_4 \) are found to be \(-1.5\%\), \(0.6^\circ\), \(-0.05^\circ\) and \(-0.05^\circ\). These parameters are used in the detector simulation and data reconstruction.

5 Spot size and variations of the number of observed photons

Photons from any given direction form a quasi-Gaussian-shaped spot on the camera, which is infected by imperfection of the mirrors surface. The spot size depends on the angular distance to the optical axis. The larger the angular distance to the optical axis, the larger the spot size and the more it deviates from a Gaussian shape due to coma of the image. The spot size as an important parameter that affects the Cherenkov images of air showers is taken into account in the ray tracing procedure in both data analysis and detector simulation.

![Fig. 4. One example of light curves in X (left) and Y (right) directions when a star passes through a PMT’s FOV.](image)

Bright stars can be considered as perfect point sources. The light from a bright star is collected by mirrors and projected to the camera, forming a light spot. The camera records the light spot in poor resolution due to the large pixel size. If a PMT is on the track of a bright star, the PMT gets brighter and brighter as the star goes nearer, dimmer and dimmer as the star leaves. If the spot size is much smaller than the track length of the star in the FOV of the PMT, the light curve recorded by the PMT will be rectangular-shaped, with the width approximately equal to the track length, while if the spot size is much larger, the light curve also will be rectangular-shaped, with the width equal to the spot size. In our case, the spot size is similar to the pixel size, the light curve becomes quasi-Gaussian-shaped.

Fig. 4 shows one example. The spot size can be estimated by fitting the light curve accordingly. In order to get rid of the affects of nearby stars, only orphan stars, which have no nearby stars within \( 2^\circ \), are used. Fig. 5 shows the variation of the spot size with angular distance to mirror axis. The spots become larger from the center of the camera to the edge. The spot size obtained from bright stars is used to improve the energy and arrival direction reconstruction.

![Fig. 5. Spot size varies with angular distance to mirror axis.](image)

Photons which fall in the insensitive areas of the camera are never recorded. In the data analysis and detector simulation, the unrecorded photons have been taken into account as part of the ray tracing procedure. This is important in shower energy estimation and tested using the stars crossing the field of view of the telescopes. When a bright star with a constant flux passes through the FOV of the camera, the number of recorded photons varies due to the different positions of the star on the camera. When the star is near to the center of a PMT, most photons fall in the sensitive areas of the camera, while when the star is near the conjunction of two PMTs, most photons fall in the insensitive areas of the camera, so the variations of the recorded photons from the star on its track can be observed which is shown in the Fig. 6. The variations are also effected by the weather conditions, so several clear nights data is used to get an average behavior of it. In the Fig. 6 the simulation of the variations along the track of the star is also shown which is consistent with the observed one.
This demonstrates that the ray tracing simulation correctly copes with the fraction of the unrecorded photons in the insensitive areas of the camera.

![Graph showing relative brightness vs. X°](image)

Fig. 6. The back squares show the variations of the observed photons on the track of a star, while the black curve shows the simulated one.

6 Conclusions

Bright stars are used as a guider to calibrate the pointing direction of each telescope and the geometry of the camera. The pointing accuracy obtained through bright stars is better than 0.05°. The long term stability of the pointing direction of the telescope is also monitored by bright stars. Moreover, as point sources, the bright stars are also used to study the spot shape. The spot size becomes larger from the center to the edge of the camera. Besides the spot size, the fraction of the unrecorded photons in the insensitive areas between PMTs is compared with the simulated one, and they are consistent with each other. The errors caused by this effect are well understood and under control in the energy reconstruction.

The pointing direction and the correction of the geometry and optics of the telescopes are used in the simulation and data analysis to improve the reconstructions of the energy and arrival direction of the air shower.

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