8-16-2019

Mechanical Resonances of Mobile Impurities in a One-Dimensional Quantum Fluid

Thomas L. Schmidt  
University of Luxembourg

Giacomo Dolcetto  
University of Luxembourg

Christopher J. Pedder  
University of Luxembourg

Karyn Le Hur  
Institut Polytechnique de Paris

Peter Orth  
Iowa State University and Ames Laboratory, porth@iastate.edu

Follow this and additional works at: https://lib.dr.iastate.edu/ameslab_manuscripts

Part of the Physics Commons

Recommended Citation
Schmidt, Thomas L.; Dolcetto, Giacomo; Pedder, Christopher J.; Le Hur, Karyn; and Orth, Peter, "Mechanical Resonances of Mobile Impurities in a One-Dimensional Quantum Fluid" (2019). Ames Laboratory Accepted Manuscripts. 479.  
https://lib.dr.iastate.edu/ameslab_manuscripts/479

This Article is brought to you for free and open access by the Ames Laboratory at Iowa State University Digital Repository. It has been accepted for inclusion in Ames Laboratory Accepted Manuscripts by an authorized administrator of Iowa State University Digital Repository. For more information, please contact digirep@iastate.edu.
Mechanical Resonances of Mobile Impurities in a One-Dimensional Quantum Fluid

Abstract
We study a one-dimensional interacting quantum liquid hosting a pair of mobile impurities causing backscattering. We determine the effective retarded interaction between the two impurities mediated by the liquid. We show that for strong backscattering this interaction gives rise to resonances and antiresonances in the finite-frequency mobility of the impurity pair. At the antiresonances, the two impurities remain at rest even when driven by a (small) external force. At the resonances, their synchronous motion follows the external drive in phase and reaches maximum amplitude. Using a perturbative renormalization group analysis in quantum tunneling across the impurities, we study the range of validity of our model. We predict that these mechanical antiresonances are observable in experiments on ultracold atom gases confined to one dimension.

Disciplines
Physics
Mechanical Resonances of Mobile Impurities in a One-Dimensional Quantum Fluid

Thomas L. Schmidt,1,* Giacomo Dolcetto,1 Christopher J. Pedder,1 Karyn Le Hur,2 and Peter P. Orth3,4

1Physics and Materials Science Research Unit, University of Luxembourg, L-1511 Luxembourg
2CPHT, CNRS, Institut Polytechnique de Paris, Route de Saclay, 91128 Palaiseau, France
3Department of Physics and Astronomy, Iowa State University, Ames, Iowa 50011, USA
4Ames Laboratory, U.S. DOE, Iowa State University, Ames, Iowa 50011, USA

(Received 24 September 2018; published 13 August 2019)

We study a one-dimensional interacting quantum liquid hosting a pair of mobile impurities causing backscattering. We determine the effective retarded interaction between the two impurities mediated by the liquid. We show that for strong backscattering this interaction gives rise to resonances and antiresonances in the finite-frequency mobility of the impurity pair. At the antiresonances, the two impurities remain at rest even when driven by a (small) external force. At the resonances, their synchronous motion follows the external drive in phase and reaches maximum amplitude. Using a perturbative renormalization group analysis in quantum tunneling across the impurities, we study the range of validity of our model. We predict that these mechanical antiresonances are observable in experiments on ultracold atom gases confined to one dimension.

DOI: 10.1103/PhysRevLett.123.075302

Introduction.—One-dimensional (1D) quantum systems have continued to fascinate condensed-matter physicists over the past decades [1,2]. They display remarkably greater universality than their higher-dimensional cousins. At the lowest energy scales, and regardless of their microscopic details, or even of whether they are composed of bosons or fermions, all gapless 1D systems can be described as Luttinger liquids (LLs) [3–5]. This hydrodynamic description is extremely simple and characterized by just two parameters: the sound velocity \(v_s\) and the Luttinger parameter \(K\). The latter determines, e.g., the compressibility, and is related to the interactions between the constituent particles.

In recent years, 1D quantum fluids have been realized on various experimental platforms, ranging from semiconductor nanowires to cold atomic gases [6–10]. Many of their predicted properties, such as conductance quantization or the presence of power laws in their response functions (with exponents determined by the interaction strength) have been observed [6,7,9,11,12]. Cold atoms, in particular, are well suited for the study of 1D systems as their interaction strength can be tuned via external magnetic fields or by changing properties of the lasers confining the atoms [9,13]. Furthermore, it was shown that impurities can be embedded into the 1D quantum fluid, either as atoms of a different species [10,14–16] or as charged ions [17,18]. Similar effects occur in the propagation of magnetic excitations along spin chains [19–22].

The effects of impurities in 1D quantum fluids are rather peculiar. It is well known that a single static impurity will cause backscattering of fluid particles. At low energies, this backscattering becomes strong for \(K < 1\), and the impurity will effectively cut the system into disconnected parts [23,24]. At finite energies, a random scattering potential caused by many static impurities leads to Anderson localization even for arbitrarily weak coupling between the impurities and the liquid [2,25]. However, these predictions apply only to the cases of static impurities and quenched disorder, respectively.

The physical properties of the system change strongly if we allow for backaction of the liquid on the impurities by giving the latter a finite mass \(M\) [26–33]. In particular, this gives rise to a new temperature scale \(T^* = (m/M)T_F\), where \(m\) is essentially the mass of the particles forming the quantum liquid and \(T_F\) the Fermi temperature [26]. For \(T^* \ll T \ll T_F\), a heavy impurity \((M > m)\) indeed cuts the system, while at even lower temperatures \(T \ll T^*\), the impurity effectively becomes transparent, in striking contrast to the infinite-mass case. The two limits can be distinguished by measuring the impurity’s mobility, i.e., its velocity as a response to an external driving force.

Considering more than a single impurity leads to even more striking effects. For static impurities, it is well known that tunneling resonances occur [23], as well as Friedel oscillations [34,35] leading to long-range interactions between two impurities. In the case of mobile impurities, the backaction of the liquid on the impurities necessarily leads to an effective retarded interaction between them. Interactions mediated by a fluid and new dynamical synchronization phenomena have been observed in a cold-atom mixture in Ref. [36]. In this Letter, we will focus on the mobility of a pair of impurities in the limit of weak tunneling of liquid particles across the impurities. We will show that as a consequence of retarded interactions between the impurities mediated by the liquid, the ac
mobility of the pair differs greatly from the mobility of individual impurities. As illustrated in Fig. 1, the behavior of the ac mobility is dominated by interference effects between density waves in the liquid and the external driving force. Such behavior is reminiscent of that underlying Fano resonances [37]; the origin of the two interfering wave fronts, however, is different in our case. The most striking consequence of this is the emergence of resonances and antiresonances in the ac mobility: at certain discrete drive frequencies, the impurity motion is reinforced or completely halted by the density waves in the fluid. We show below that these features of the mobility at finite frequencies can be experimentally observed by measuring the absorption spectrum for electromagnetic radiation.

The resonance phenomena that we discover have the following properties: First, it is crucial that the system is one-dimensional because a dispersion of the density waves into other directions would destroy the exact interference of the external force with the force due to the density wave emitted from the second impurity. Second, the resonances and antiresonances are retardation phenomena which rest on the finiteness of the sound velocity in the LL and the finite distance between impurities. Third, the leading correction causing a partial lifting of the resonances is brought about by quantum mechanics: both via tunneling of the liquid across the impurities to explore the limits of validity of the model.

Effective action.—We begin by presenting a model Hamiltonian to investigate a pair of mobile impurities interacting with an LL. The Hamiltonian \( H \) of the system divides into three parts, \( H = H_{LL} + H_{imp} + H_{int} \), which describe the low-energy modes of the liquid, the dynamics of the mobile impurities, and the coupling between the two, respectively. \( H_{LL} \) is the usual Luttinger Hamiltonian [2] (in the following, we set \( \hbar = k_B = 1 \)),

\[
H_{LL} = \frac{v_s}{2\pi} \int dx \left[ K(\partial_x \theta)^2 + \frac{1}{K} (\partial_x \phi)^2 \right],
\]

where \( v_s \) is the sound velocity of the fluid modes, and \( K \) is the Luttinger parameter, which for repulsive interactions in a fermionic system takes values \( 0 < K < 1 \). The fields \( \phi \) and \( \theta \) obey the canonical commutation relation \([\phi(x), \partial_y \theta(y)] = i\pi \delta(x-y)\).

The kinetic energy of the mobile impurities can be written in center-of-mass (c.m.) and relative (r) coordinates as \( H_{imp} = P_{c.m.}^2/(2M) + P_r^2/(2\mu) \), where \( M \) and \( \mu \) are the total and reduced mass of the two impurities, respectively. Finally, we allow for a contact interaction between the impurities and the Luttinger modes which is of the form

\[
H_{int} = V \sum_{\eta=\pm} \rho(X_{c.m.} + \eta X_r/2),
\]

where \( \rho(x) = -\partial_x \phi(x)/\pi + 2\rho_0 \cos(2\pi \rho_0 x - 2\phi(x)) \) is the density of the LL, which consists of a forward scattering and a backscattering contribution [38]. Moreover, \( X_{c.m.} \) and \( X_r \) are the center-of-mass and relative coordinates of the impurity pair.

We transform to a frame comoving with the center of mass of the system using the unitary transformation \( U = \exp[iX_{c.m.} P_{LL}] \). Here, \( P_{LL} = \int dx (\partial_x \theta)(\rho_0 - \partial_x \phi/\pi) \) is the momentum of the LL, where \( \rho_0 = N/L \) denotes the average density. Under this transformation, the Hamiltonian becomes \( H' = U^\dagger H U \), where

\[
H' = \left( \frac{P_{c.m.}^2 - P_{LL}^2}{2M} \right) + \frac{P_r^2}{2\mu} + H_{LL} + \sum_{\eta=\pm} V \rho(\eta X_r/2).
\]
impurities, the most straightforward way to implement such a drive is via a time-dependent electric field with wavelength $\lambda \gg d$, as both impurities will experience the same driving force in this case. In case of neutral atoms, one can define impurities by using different species of atoms. The necessary species-dependent trapping potentials for driving them can be routinely realized[10,39,40].

Second, we consider the limit of strong backscattering by the impurities ($V \to \infty$), which leads to complete pinch-off of the LL at the impurities. This is justified because the impurities act as RG-relevant perturbations. We will discuss this assumption later by presenting an RG calculation of the LL at the impurities. This is justified because the strong nonlinearity present in the interaction Hamiltonian (2) has been translated into boundary conditions of the field $\theta(x)$, frequency $\Omega$ is defined as $\omega/\Omega_\infty$, and $\mu(\omega) = \mu_0$, one finds that the boundary conditions provided by the LL have a strong impact on it. The center-of-mass mobility as a function of Matsubara frequency is defined as $\mu(\omega_n) = \mu(\omega_n/\beta) \langle |\tilde{X}_{c.m.}(\omega_n)|^2 \rangle$. Computing the expectation value, and passing back to real frequencies by making the Wick rotation $\omega_n \to -i\omega + 0^+$, we find that

$$
\mu(\omega) = \left\{ 1 - i \left[ \frac{\omega}{\Omega_M} + \tan \left( \frac{\omega}{2\Omega_d} \right) \right] \right\}^{-1}.
$$

It is clear from this expression that the mobility exhibits resonances for $\omega/\Omega_M + \tan(\omega/2\Omega_d) = 0$, where it reaches the dc value: $\mu(\omega) = \mu_0$. Interestingly, it also exhibits antiresonances for $\omega/\Omega_M + \tan(\omega/2\Omega_d) \to \infty$, where $\mu(\omega) = 0$. The full behavior of $\mu(\omega)$ is shown in Fig. 2, which shows that the mobility of the impurity pair is very different from that of a single impurity, except at certain discrete frequencies, where they agree.

To understand the form of $\mu(\omega)$, note that the ac drive causes the impurities to emit sound waves into the quantum liquid [26]. The antiresonances are reached exactly when the tangent function diverges, i.e., for $\omega = n\pi\Omega_d$ with odd $n$. This corresponds to situations where the driving force at, say, the right impurity and the wave front arriving with retardation $\Omega_d^{-1} = d/v_d$ from the left impurity interfere destructively. In that case, the forces cancel and the impurities will remain at rest despite the drive, so that $\mu = 0$.

Further increasing the frequency $\omega$, one reaches a point when the external driving force on the impurities and the force due to absorption and emission of liquid density waves conspire in such a way that the impurity motion is always exactly in phase with the external drive, even at finite frequency. This requires that the acceleration of the impurity vanishes exactly at the time when the external force changes direction. In this case, the dc mobility is restored, and the oscillation amplitude as well as the power absorption reach a maximum (see Fig. 2). This is a striking contrast to the case of a single impurity, where the motion is always phase shifted with respect to the ac drive.
Our previous analysis of $\mu(\omega)$ corresponding to even multiples of $\pi\Omega_0$, the two forces interfere constructively, and the mobility for finite $d$ coincides with that of $d=0$. Hence, the two impurities behave identically to a single impurity as far as the mobility is concerned.

**Real-time dynamics.**—In order to get a complete physical understanding of the system, we investigate the center-of-mass dynamics of the impurities in the time domain. The velocity of the center of mass is given by

$$v_{c.m.}(t) = \frac{d}{2\pi} \int e^{i\omega t} \mu(\omega) \tilde{F}(\omega),$$

where $\tilde{F}(\omega) = \int dt e^{i\omega t} F(t)$ is the applied force in the frequency domain. From Eq. (7), one finds that $\mu(\omega) = \mu^*(-\omega)$ and that the singularities of $\mu(\omega)$ are in the lower complex half-plane, so $v_{c.m.}(t)$ is assured to be real and respect causality.

Our previous analysis of $\mu(\omega)$ in the frequency domain immediately yields the real-time center-of-mass dynamics of the impurity pair for the case of a harmonically driven system, where $F(t) = F_0 \sin(\omega t)$,

$$v_{c.m.}(t) = F_0 |\mu(\omega)| \sin[\omega t - \phi(\omega)],$$

where we have split the mobility into its absolute value and phase using $\phi(\omega) = \arg[\mu(\omega)]$. According to Fig. 2, when $\omega$ is on resonance, the velocity $v_{c.m.}(t)$ oscillates in phase with the external force and with the maximum amplitude, $v_{c.m.}(t) = F_0 \mu_0 \sin(\omega t)$. By contrast when $\omega$ hits an antiresonance, we find $v_{c.m.}(t) = 0$ at all times. Near the antiresonances, the relative phase of the center-of-mass velocity with respect to the external drive changes from $\pi/2$ to $-\pi/2$. In the case of a periodic drive, the mobility can most easily be measured by studying the power absorbed by the impurities over a drive period $T = 2\pi/\omega$,

$$\tilde{P}(\omega) = \frac{1}{T} \int_0^T dt F(t) v_{c.m.}(t) = \frac{1}{2} F_0^2 |\mu(\omega)| \cos[\phi(\omega)].$$

(10)

Hence, the resonances and antiresonances in Fig. 2 are directly measurable, for instance, as the power absorption by the impurities driven by an external electric field or modulated species-selective trapping potential.

The drive force acting identically on the two impurities allowed us to neglect their relative motion [38]. However, due to the fluctuation-dissipation theorem, the dissipation caused by the liquid is accompanied by fluctuating forces acting on the individual impurities which increase with temperature [41], thus potentially reducing the visibility of the resonances at high temperatures. In the Supplemental Material [38], we estimate this temperature scale to be of order $T_F^2/\omega$. Hence, for $\omega < T_F$, the resonances will remain visible at all temperatures $T \ll T_F$.

We expect that our predictions can most conveniently be measured in ultracold atom gases in one-dimensional traps [9,13]. In this case, with typical sound velocities in the range of mm/s and distances between impurities on the order of $\mu$m, the resonance phenomena should be visible in the electromagnetic absorption at kHz frequencies. With typical Fermi temperatures in the $\mu$K range, the condition $\omega < T_F$ is thus fulfilled, and the predicted features should be observable in the entire temperature range $T^* \ll T \ll T_F$, where impurity backscattering is relevant.

**RG analysis.**—To obtain these results, we assumed the two impurities to pinch off the liquid at the positions $\pm d/2$. The leading perturbations to this strong-pinning limit are described by adding terms to the action (5) corresponding to tunneling across the individual impurities and across the impurity pair. These are given by the respective actions

$$S_{\text{tun.1}} = -t_1 \sum_{a=L,R} \int d\tau \cos[\theta_{a+}(\tau) - \theta_{a-}(\tau)],$$

$$S_{\text{tun.2}} = -t_2 \int d\tau \cos[\theta_{R+}(\tau) - \theta_{L-}(\tau)].$$

(11)

We perform an RG analysis for these terms by splitting the bosonic modes into slow modes and fast modes, and integrating out the fast modes [2]. The RG flow of the running LL cutoff $\Lambda$ depends on the energy $\Omega_0 = v_s/d$, corresponding to the distance between the impurities, as

FIG. 2. Comparison between the ac mobility $\mu(\omega)$ [Eq. (7)] and absorbed power $\tilde{P}(\omega)$ [Eq. (10)] of one impurity ($d=0$, red curve) and two impurities ($d=2v_s/\Omega_0$, blue curve) as a function of frequency. Top panel: absolute value of $\mu(\omega)$ and $\tilde{P}(\omega)$ normalized with respect to their maxima. Lower panel: complex phase of $\mu(\omega)$. For a single impurity, the mobility decreases monotonically with $\omega$ while the phase monotonically increases from zero to $\pi/2$. In contrast, for two impurities one finds a series of resonances where $\mu(\omega) = \mu_0$ and $\arg(\mu) = 0$, as well as antiresonances where $\mu(\omega) = 0$ and $\arg(\mu) = \pm \pi/2$.

075302-4
well as $\Omega_M = 2\pi p^2/(KM)$, corresponding to the mass of the impurities.

In the limit of large $d$, we find the following RG flows for the cases of heavy ($M \to \infty$) and light ($M \to 0$) impurities, respectively,

$$\frac{dt_{1,2}}{d\xi} = \left[ 1 - \frac{1}{K} \right] t_{1,2}, \quad \Omega_d \ll \Omega_M \ll \Lambda,$$

$$\frac{dt_{1,2}}{d\xi} = \left[ 1 - \frac{1}{2K} \right] t_{1,2}, \quad \Omega_d \ll \Lambda \ll \Omega_M. \quad (12)$$

The tunneling amplitudes $t_1$ and $t_2$ scale identically. The first line coincides with the result for static impurities [23] and shows that tunneling is irrelevant for $K < 1$ for heavy impurities until $\Lambda$ falls below $\Omega_d$. $\Omega_M$ [see Eq. (13) below]. Interestingly, for light impurities, the second line shows that in this regime of large $d$, tunneling is relevant for $1/2 < K < 1$, in contrast to the static case. If the interactions in the LL are not too strong, light impurities thus become transparent even though they are far apart. For sufficiently strong interactions $K < 1/2$, tunneling remains irrelevant as long as $T > \Omega_d$. This central, new result of our RG analysis implies that the resonance phenomena discussed in the previous section remain robust to quantum tunneling across the impurities for sufficiently strong interactions in the LL ($K < 1/2$) and not too low temperatures $T > T^*$ for $M > m$ and $T > \Omega_d$ for $M < m$.

We note that the scaling dimension of $1/(2K)$ for two light impurities generalizes to $(N - 1)/(NK)$ for $N$ light impurities. This factor arises from the existence of a single gapped mode in the limit $\Omega_M \to \infty$, which reads $\theta_{L} = \theta_{L+} + \theta_{R} - \theta_{R+}$ for $N = 2$ and generalizes straightforwardly to general $N$. The other $2N - 1$ orthogonal modes remain gapless. As the gapping of this mode occurs only in the approximation of keeping $X_d = d$ constant, we conclude that the (quantitative) scaling dimension $1/(2K)$ is not universal and would change if we allowed relative motion of the impurities. We expect the mean qualitative conclusion, however, that pairs of light impurities with large $d$ become transparent at a smaller value of $K$ than single impurities, to remain valid.

To connect to the existing results for a single mobile impurity, we need to consider the case $d \to 0$. In that case, the bosonic modes $\theta_{L+}$ and $\theta_{R+}$, which live between the impurities, are pushed to high energies. As a consequence, the RG calculation predicts that the tunneling amplitude $t_1$ is exponentially suppressed at energies $\Lambda \ll \Omega_d$. In contrast, the tunneling amplitude $t_2$ remains finite and, in the limits of heavy and light impurities, respectively, scales as

$$\frac{dt_2}{d\xi} = \left[ 1 - \frac{1}{K} \right] t_2, \quad \Omega_M \ll \Lambda \ll \Omega_d,$$

$$\frac{dt_2}{d\xi} = t_2, \quad \Lambda \ll \Omega_M \ll \Omega_d. \quad (13)$$

Hence, we recover the typical scaling in the limit of heavy impurities [23]. Moreover, in the limit of light impurities and $d \to 0$, tunneling becomes relevant irrespective of interaction strength. This coincides with the result found in Ref. [26] for a single mobile impurity.

Conclusions.—In this Letter, we have shown that a pair of mobile impurities embedded in a Luttinger liquid can display rich physical behavior. In particular, we showed that interference effects between an external driving force and forces caused by density waves that are generated in the liquid as a response, can enhance or attenuate the mobility of the center-of-mass motion of the two impurities. In the extreme case, antiresonances arising from the destructive interference between external and Luttinger liquid mediated forces can render the impurity pair completely immobile at certain discrete frequencies. We argued that our predictions can be measured in ultracold atom gases in one-dimensional traps. We estimated that resonances and antiresonances should be visible in the kHz range in a temperature window given by $(m/M)T_F < T < T_{c1}$ where $m/M < 1$ is the mass ratio between liquid particles and the heavy impurities and $T_F$ is the Fermi temperature.

T. L. S., G. D., and C. J. P. acknowledge support by the Fonds National de la Recherche Luxembourg under grant ATTRACT 7556175. P. P. O. acknowledges support from Iowa State University Startup Funds. K. L. H. acknowledges support by the Deutsche Forschungsgemeinschaft via Grant No. DFG FOR2414 and by the LABEX PALM Grant No. ANR-10-LABX-0039, as well as discussions at the CIFAR meeting in Canada on quantum materials.

\*thomas.schmidt@uni.lu

[1] A. O. Gogolin, A. A. Nersesyan, and A. M. Tsvelik, Bosonization and Strongly Correlated Systems (Cambridge University Press, Cambridge, England, 1998).

[2] T. Giamarchi, Quantum Physics in One Dimension (Clarendon Press, Oxford, 2003).

[3] S. Tomonaga, Prog. Theor. Phys. 5, 544 (1950).

[4] J. M. Luttinger, J. Math. Phys. (N.Y.) 4, 1154 (1963).

[5] F. D. M. Haldane, J. Phys. C 14, 2585 (1981).

[6] O. M. Auslaender, H. Steinberg, A. Yacoby, Y. Tserkovnyak, B. I. Halperin, K. W. Baldwin, L. N. Pfeiffer, and K. W. West, Science 308, 88 (2005).

[7] H. Steinberg, G. Barak, A. Yacoby, L. N. Pfeiffer, K. W. West, B. I. Halperin, and K. Le Hur, Nat. Phys. 4, 116 (2008).

[8] G. Barak, H. Steinberg, L. N. Pfeiffer, K. W. West, L. Glazman, F. von Oppen, and A. Yacoby, Nat. Phys. 6, 489 (2010).

[9] I. Bloch, J. Dalibard, and W. Zwerger, Rev. Mod. Phys. 80, 885 (2008).

[10] F. Meinert, M. Knap, E. Kirillov, K. Jag-Lauber, M. B. Zvonarev, E. Demler, and H.-C. Nägerl, Science 356, 945 (2017).
[11] M. Bockrath, D. H. Cobden, J. Lu, A. G. Rinzler, R. E. Smalley, L. Balents, and P. L. McEuen, Nature (London) 397, 598 (1999).

[12] H. Ishii, Nature (London) 426, 540 (2003).

[13] S. Giorgini, L. P. Pitaevskii, and S. Stringari, Rev. Mod. Phys. 80, 1215 (2008).

[14] S. Palzer, C. Zipkes, C. Sias, and M. Köhl, Phys. Rev. Lett. 103, 150601 (2009).

[15] N. Spethmann, F. Kindermann, S. John, C. Weber, D. Meschede, and A. Widera, Phys. Rev. Lett. 109, 235301 (2012).

[16] J. Catani, G. Lamporesi, D. Naik, M. Gring, M. Inguscio, F. Minardi, A. Kantian, and T. Giamarchi, Phys. Rev. A 85, 023623 (2012).

[17] C. Zipkes, S. Palzer, C. Sias, and M. Köhl, Nature (London) 464, 388 (2010).

[18] C. Sias and M. Köhl, arXiv:1401.3188v1.

[19] M. B. Zvonarev, V. V. Cheianov, and T. Giamarchi, Phys. Rev. Lett. 99, 240404 (2007).

[20] M. B. Zvonarev, V. V. Cheianov, and T. Giamarchi, Phys. Rev. Lett. 103, 110401 (2009).

[21] T. Fukuhara, A. Kantian, M. Endres, M. Cheneau, P. Schauß, S. Hild, D. Bellem, U. Schollwöck, T. Giamarchi, C. Gross, I. Bloch, and S. Kuhr, Nat. Phys. 9, 235 (2013).

[22] A. Imambekov, T. L. Schmidt, and L. I. Glazman, Rev. Mod. Phys. 84, 1253 (2012).

[23] C. L. Kane and M. P. A. Fisher, Phys. Rev. B 46, 15233 (1992).

[24] C. L. Kane and M. P. A. Fisher, Phys. Rev. Lett. 68, 1220 (1992).

[25] T. Giamarchi and H. J. Schulz, Phys. Rev. B 37, 325 (1988).

[26] A. H. Castro Neto and M. P. A. Fisher, Phys. Rev. B 53, 9713 (1996).

[27] A. Lamacraft, Phys. Rev. B 79, 241105(R) (2009).

[28] M. Schecter, D. Gangardt, and A. Kamenev, Ann. Phys. (Amsterdam) 327, 639 (2012).

[29] C. J. M. Mathy, M. B. Zvonarev, and E. Demler, Nat. Phys. 8, 881 (2012).

[30] F. Massel, A. Kantian, A. J. Daley, T. Giamarchi, and P. Törnä, New J. Phys. 15, 045018 (2013).

[31] M. Schecter and A. Kamenev, Phys. Rev. Lett. 112, 155301 (2014).

[32] M. Knap, C. J. M. Mathy, M. Ganahl, M. B. Zvonarev, and E. Demler, Phys. Rev. Lett. 112, 015302 (2014).

[33] M. Schecter, D. M. Gangardt, and A. Kamenev, New J. Phys. 18, 065002 (2016).

[34] K. A. Matveev, D. Yue, and L. I. Glazman, Phys. Rev. Lett. 71, 3351 (1993).

[35] R. Egger and H. Grabert, Phys. Rev. Lett. 75, 3505 (1995).

[36] M. Delehaye, S. Laurent, I. Ferrier-Barbut, S. Jin, F. Chevy, and C. Salomon, Phys. Rev. Lett. 115, 265303 (2015).

[37] M. O. Scully and M. S. Zubairy, Quantum Optics (Cambridge University Press, Cambridge, England, 1997).

[38] See Supplemental Material at http://link.aps.org/supplemental/10.1103/PhysRevLett.123.075302 for a detailed study of a solvable classical model which shows the same features as the quantum impurity problem studied in the main text. It also contains a discussion of the effect of thermal fluctuations on the visibility of the resonance features.

[39] L. J. LeBlanc and J. H. Thywissen, Phys. Rev. A 75, 053612 (2007).

[40] B. Gadway, D. Pertot, R. Reimann, and D. Schneble, Phys. Rev. Lett. 105, 045303 (2010).

[41] U. Weiss, Quantum Dissipative Systems (World Scientific, Singapore, 1999).