Impact of doping on the carrier dynamics in graphene

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We present a microscopic study on the impact of doping on the carrier dynamics in graphene, in particular focusing on its influence on the technologically relevant carrier multiplication in realistic, doped graphene samples. Treating the time- and momentum-resolved carrier-light, carrier-carrier, and carrier-phonon interactions on the same microscopic footing, the appearance of Auger-induced carrier multiplication up to a Fermi level of 300 meV is revealed. Furthermore, we show that doping favors the so-called hot carrier multiplication occurring within one band. Our results are directly compared to recent time-resolved ARPES measurements and exhibit an excellent agreement on the temporal evolution of the hot carrier multiplication for n- and p-doped graphene. The gained insights shed light on the ultrafast carrier dynamics in realistic, doped graphene samples.

A number of theoretical and experimental studies has been performed aiming at a thorough understanding of the carrier relaxation dynamics in optically excited graphene\textsuperscript{1–15}. Most of these studies focus on the ultrafast Coulomb- and phonon-induced carrier dynamics without considering the influence of doping in the investigated graphene samples. A non-zero Fermi level can have a crucial impact on the relaxation dynamics via a significant increase of the scattering phase space and via the enhancement of Pauli blocking. A first experimental time-resolved ARPES study has been performed addressing the doping dependence of carrier multiplication of graphene\textsuperscript{16}. The underlying elementary processes determining the observed different behavior for p- and n-doped samples have not been microscopically investigated, yet.

In this work, we apply a microscopic approach to access the time-, momentum-, and angle-resolved dynamics of electrons and phonons in optically excited graphene under the influence of a variable n- and p-doping. The focus lies in particular on the impact of a finite Fermi level on the appearance of the technologically relevant carrier multiplication\textsuperscript{16–27}. This interesting ultrafast phenomenon is related to the linear electronic band structure of graphene opening up the possibility of efficient Coulomb-induced Auger processes. A significant multiple carrier generation has been theoretically predicted\textsuperscript{17,19,26} and experimentally confirmed in graphene\textsuperscript{16,21,22,25,27}. So far, the theoretical studies have been constrained to the case of undoped graphene. Introducing a non-zero Fermi level in graphene, electrons above the Dirac point or above the Fermi level can be considered as charge carriers (holes in analogy). In the first case, the carrier multiplication can take place via Auger scattering bridging the valence and the conduction band. In the following, we label this process as carrier multiplication (CM). On the other side, counting carriers with respect to the Fermi level, the multiplication occurs via Coulomb-induced intraband scattering bridging the states below and above the Fermi level, cf. Fig. 1. According to literature\textsuperscript{21}, we label this process as hot carrier multiplication (hCM). Here, the actual number of charge carriers remains unchanged in each band. Nevertheless, since these hot carriers are crucial for many technological applications, the appearance of hCM is also of technological relevance.

**Theoretical approach**

The starting point for the calculation is the many-particle Hamilton operator $H = H_0 + H_{cl} + H_{cp} + H_{cc}$, where $H_0$ denotes the interaction-free carrier and phonon part, $H_{cl}$ the carrier-light coupling, $H_{cp}$ the carrier-phonon interaction, and $H_{cc}$ the carrier-carrier interaction\textsuperscript{28}. The carrier dynamics is described...
by graphene Bloch equations\(^1\) corresponding to a coupled set of differential equations for the occupation probability \(\rho_k^\lambda(t)\) in the state \(k\) and the band \(\lambda = (v, c)\), the microscopic polarization \(\rho_k(t)\) that is a measure for the optical transition probability between both bands, and the phonon occupation \(n_q^{\lambda}(t)\) with the momentum \(q\) for different optical and acoustic phonon modes\(^29\):

\[
\dot{\rho}_k^\lambda(t) = (i\epsilon_k^\lambda + i(\Omega_k^\lambda - \Omega_k^\lambda) - \gamma_k)\rho_k^\lambda(t) + B_k^\lambda(t)\rho_k(t) + \rho_k(t),
\]

\[
\dot{\rho}_k(t) = \pm 2\Omega_k^\lambda \rho_k^\lambda(t) + \Gamma_{in}^\lambda(t)(1 - \rho_k^\lambda(t)) - \Gamma_{out}^\lambda(t)\rho_k^\lambda(t),
\]

\[
\dot{n}_q^\lambda(t) = -\gamma_ph\left(n_q^\lambda(t) - n_{\text{ph}}^\lambda(t)\right) + \Gamma_{em,\text{abs}}^\lambda(t)\left(1 + n_q^\lambda(t)\right) - \gamma_{\text{ph}}^\lambda n_q^\lambda(t).
\]

Here, \(\epsilon_k^\lambda = \frac{1}{\hbar}(\epsilon_k^v - \epsilon_k^c)\) is the optical transition frequency within the linear electronic band structure \(\epsilon_k^\lambda\) of graphene close to the Dirac point. The carrier-light coupling is determined by \(\Omega_k^\lambda(t)\) that is a measure for the optical transition probability between both bands, and the phonon occupation \(n_q^\lambda(t)\) with the momentum \(q\) for different optical and acoustic phonon modes. The microscopic polarization is pumped by the many-particle-induced diagonal dephasing \(\gamma_k(t)\) and is driven by the off-diagonal dephasing term \(\gamma_{\text{ph}}(t)\). The equation of motion for the phonon occupation \(n_q^\lambda(t)\) is obtained and contains phonon emission and absorption rates \(\Gamma_{em,\text{abs}}^\lambda(t)\). The finite phonon lifetime\(^32\) \(\gamma_{\text{ph}}\) is considered by a coupling to a phonon bath \(n_{\text{ph}}^\lambda\) at room temperature. The explicit form of the time- and momentum-dependent scattering rates is discussed in the supplementary material. More details on the diagonal and off-diagonal dephasing terms can be found in Malic et al.\(^29\).

A finite Fermi level \(E_F\) breaks the symmetry between the valence and conduction band around the Dirac point, cp. Fig. 1. As a result, the occupation probability of electrons \(\rho_k^h = \rho_k^v\) and of holes \(\rho_k^h \neq 1 - \rho_k^v\) needs to be treated separately. As initial condition, we assume a Fermi distribution \(\rho_k^{(e/h)} = \left[\exp\left(\frac{\epsilon_k^{(e/h)} - E_F}{k_B T}\right) + 1\right]^{-1}\), where + stands for the hole and − for the electron occupation at the temperature \(T\). Another important aspect of doping is the increased screening of the Coulomb interaction. The bare Coulomb potential \(V_q\) appearing in the Coulomb-induced scattering rates \(\Gamma_{kin,\text{out}}^\lambda(t)\) is screened via the dynamic dielectric function \(\varepsilon(q, \omega)\) that is defined by the Lindhard equation\(^28,33\), cf. the supplementary material for a more detailed discussion. Since this many-particle-induced screening is directly influenced by carrier occupations in the conduction and valence bands, doping plays a crucial role and has a significant influence on the ultrafast carrier dynamics in graphene.

With the presented microscopic approach, we can track the relaxation dynamics of non-equilibrium charge carriers in time, and energy including the temporal evolution of the carrier density after the
optical excitation. First, we focus on the electron and hole dynamics in highly doped graphene and then we discuss the impact of doping on the appearance of carrier multiplication.

Results and Discussion

Electron and hole dynamics. Here, we discuss how the doping-induced symmetry breaking between electrons in the conduction band and holes in the valence band influences the dynamics of optically excited charge carriers in realistic doped graphene samples. Figure 2 illustrates the angle-averaged occupation probability $\rho_{\mathbf{k}}^c$ for (a) electrons and (b) holes for an initial Fermi level of 300 meV as a function of the carrier energy for different times after the optical excitation. Note that due to the n-doping the electron relaxation is faster resulting in a thermalized hot Fermi distribution already after 30 fs. The inverse behavior can be found for p-doped graphene.

Carrier multiplication (CM). Now, we study the impact of an initial Fermi level $E_F$ on the Coulomb-induced multiple carrier generation, which is generally defined as the ratio between the number of overall generated electron-hole pairs and the optically excited charge carriers

$$\langle h \rangle CM = \frac{n - n_T}{n_{\text{opt}}},$$

where $n$ is the total carrier density, $n_T$ the initial thermal carrier background, and $n_{\text{opt}}$ the optically excited carrier density. All contributions contain both electrons in the conduction band as well as holes in the valence band. For doped graphene, the specific definition depends on the physical situation: For optical measurements probing vertical carrier transitions, a definition with respect to to the Dirac point is reasonable, i.e. $\rho_{\mathbf{k}}^c = \rho_{\mathbf{k}}^c$ and $\rho_{\mathbf{k}}^h = 1 - \rho_{\mathbf{k}}^c$. The carrier density then reads

$$n = \frac{\sigma_{\text{c}} \sigma_{\text{v}}}{L^2} \sum_{\lambda=c,h,k} \rho_{\mathbf{k}}^\lambda,$$
where $L^2$ is the graphene area and $\sigma$ ($\sigma_v$) denotes the spin (valley) degeneracy. On the other side, electric transport phenomena are also of great interest, where hot electrons around the Fermi level are relevant giving rise to a hot carrier multiplication, cf. Fig. 1. This situation will be discussed in the next section.

Treating the full set of graphene Bloch equations, we have microscopic access to the temporal evolution of the carrier density including the contributions of carrier-light, carrier-carrier, and carrier-phonon interactions. Figure 3(a) illustrates the temporal evolution of CM as a function of the initial Fermi level $E_F$ at a fixed absorbed pump fluence of $0.3 \mu J/cm^2$. The surface plot reveals that doping clearly reduces the CM efficiency: The lower $E_F$, the higher is the CM factor reaching values of up to approximately 1.7 for undoped graphene at the considered pump fluence, cf. Fig. 3(b). CM can be observed for $EF$ of up to 300 meV. It occurs on a timescale of up to 150 fs for undoped graphene and becomes significantly shorter for increasing doping, as illustrated in Fig. 3(c).

The observed CM in the low-doping case can be explained by the strongly efficient impact excitation (IE) prevailing over the inverse process of Auger recombination (AR), which is a result of the large gradient in carrier occupation around the Dirac point, cf. Fig. 2(a). For undoped graphene, the probability for IE can be written as $\rho^v(1-\rho^c) \approx 1$, whereas the probability for AR is given by $\rho^c(1-\rho^v) \approx 0$ (since $\rho^c \approx 1$ and $\rho^v \approx 0$). In this case, IE is significantly favored by Pauli blocking during the initial dynamics. This is reflected by the corresponding rates $\gamma_{IE}$ and $\gamma_{AR}$ that are shown in Fig. 4(a). We observe that the IE rate is clearly higher for a time range of approximately 100 fs determining the strength of the appearing CM. During the carrier relaxation both rates converge to the same value and end up in an equilibrium, where no more carriers are generated. The timescale of the CM is determined by the duration of the imbalance between IE and AR rates in combination with the interplay with competing channels of carrier-phonon scattering, which transfer energy from the electronic system to the lattice. With an increasing doping, Auger scattering becomes more and more Pauli blocked resulting in overall lower rates, cf. Fig. 4(b). For Fermi levels higher than 300 meV, AR becomes the dominant relaxation channels and CM does not appear anymore.

**Hot carrier multiplication (hCM).** Now, we focus on the situation, where charge carriers are defined with respect to the Fermi level, i.e. for n-doped graphene the upper Dirac cone is split into $\rho^o_{k} \equiv \rho^o_{k} \approx \rho^o_{k}$ for $k > k_F$ and $\rho^o_{k} \equiv \rho^o_{k} = 1 - \rho^o_{k}$ for $k < k_F$ with the Fermi momentum $k_F$. The bottom cone remains unaffected with $\rho^o_{k} \equiv \rho^o_{k} = 1 - \rho^o_{k}$. The according hot carrier density $\bar{n}$ is given by
\[ \sum_{\sigma} \sum_{\rho} \rho(\sigma) \rho(\bar{\sigma}) = \left( \sum_{k} \rho_{k}^{h} + \sum_{k} \rho_{k}^{e} \right) + \sum_{k} \rho_{k}^{h,e} \right), \]

and the associated hot carrier multiplication is highly relevant for transport phenomena, cf. Fig. 1. Note that we obtain symmetric results for n- and p-doped graphene, since the contribution of both electrons and holes to the carrier density is considered. For undoped graphene, both definitions of carrier density [Eqs. (5) and (6)] and carrier multiplication are equivalent for symmetry reasons.

The surface plot in Fig. 5(a) illustrates hCM as a function of the Fermi level \( E_F \) and time at a fixed absorbed pump fluence of \( \varepsilon_{\text{abs}} = 0.3 \mu \text{J/cm}^2 \). In contrast to the behavior of CM, we observe a clear increase of hCM with doping. We reach hCM factors of up to approximately 2 (at the considered pump fluence) on a timescale of about 200 fs for highly doped graphene with \( E_F = 300 \text{ meV} \), cf. Fig. 5(b,c). There is nearly a linear dependence between hCM and doping: The smaller \( E_F \), the less pronounced is hCM, and the faster it decays. The probability for intraband IE processes is given by \( \rho^{h,e}(1 - \rho^{h,e}) \), which is initially large compared to the probability for intraband AR processes \( \rho^{h,e}(1 - \rho^{h,e}) \), cf. Fig. 1. With the increasing Fermi level, the intraband Auger processes are shifted into a region of higher density of states making them more efficient, as reflected by the much higher scattering rates displayed in Fig. 4(b). The initial strong imbalance between \( \gamma_{\text{AR}} \) and \( \gamma_{\text{IE}} \) gives rise to a pronounced hCM.

Besides the discussed doping dependence, CM or hCM are strongly sensitive to the excitation regime. A detailed discussion is provided in the supplementary material, where a semi-analytical approach is presented focusing on the purely Coulomb-induced CM and hCM.

**Direct comparison to experimental data.** After having presented the theoretical results on the doping dependence of the carrier multiplication, we perform a direct comparison with recently performed time-resolved ARPES measurements on n- and p-doped graphene samples. We explicitly take into account the experimental conditions, such as the Fermi level and the excitation strength. Considering that our microscopic theory does not contain any fitting parameters, we obtain an excellent agreement between theory and experiment, cf. the inset in Fig. 5(c). There is a clearly higher hCM for n-doped graphene reaching values of up to 2.2 in the theory and more than 3 in the experiment. In contrast, for p-doped graphene only a small hCM of 1.4 or 1.2 is obtained in theory and experiment, respectively. This pronounced difference is not due to the type of doping (n, p), as one might assume. It can be clearly explained by the differences in the applied fluence \( \varepsilon_{\text{abs}} \) and the actual Fermi level \( E_F \). Note that at the exactly same conditions with respect to \( E_F \) and \( \varepsilon_{\text{abs}} \), we obtain the same hot carrier multiplication for both n- and p-doped samples. However, the experiment has been performed for: (i) n-doped graphene with the Fermi level \( E_F = 380 \text{ meV} \) and an absorbed pump fluence
of $\varepsilon_{abs} = 0.5 \mu$Jcm$^{-2}$ and (ii) p-doped graphene with $E_F = 240$ meV and $\varepsilon_{abs} = 1.5 \mu$Jcm$^{-2}$. As shown in Fig. 5(b), hot carrier multiplication increases almost linearly with the Fermi level. Furthermore, it is strongly suppressed in the strong excitation regime, i.e. the larger the pump fluence, the less efficient is the hCM, as illustrated in Fig. S3 in the supplementary material. As a result, the n-doped graphene sample shows a much more pronounced hCM, since its Fermi level is significantly higher and since the experiment has been performed at a clearly smaller pump fluence compared to the p-doped graphene sample.

While the theory qualitatively reproduces well the experimental data, quantitatively, it underestimates the CM value in the first 50 fs as well as its temporal decay in the n-doped case. This might be due to the applied semi-Markovian description of the CM processes. A full non-Markovian approach would allow for a dynamical build-up of the screening of the Coulomb interaction and would lead to more allowed scattering channels on short time scales. Another possible reason for the deviation in the first 50 fs is that the experimental estimate of the carrier density is based on the introduction of a carrier temperature. However, the latter can only be well defined once a thermalized carrier distribution is reached, which occurs during that timescale. The faster temporal decay of the CM in the experiment could also be explained by the occurrence of additional scattering channels in a non-Markovian description or might suggest an additional impurity-induced scattering channel that accelerates the CM decrease.

In conclusion, we have presented a microscopic study of the carrier dynamics in doped graphene samples, in particular focusing on the impact of a finite Fermi level on the (hot) carrier multiplication. We reveal the appearance of Auger-induced carrier multiplication up to Fermi levels of 300 meV. In the case of the hot carrier multiplication occurring within one band doping is even advantageous, since it increases the phase space by providing a large number of available scattering partners. Finally, we have directly compared our results to recent time-resolved ARPES measurements finding an excellent agreement and providing a microscopic explanation for the observed different behavior in n- and p-doped graphene samples. Our results contribute to a better understanding of the ultrafast carrier dynamics in realistic graphene samples and give valuable insights into the technologically relevant carrier multiplication in graphene.
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