Joint Resource Allocation and Configuration Design for STAR-RIS-Enhanced Wireless-Powered MEC

Xintong Qin, Zhengyu Song, Member, IEEE, Tianwei Hou, Member, IEEE, Wenjuan Yu, Member, IEEE, Jun Wang, and Xin Sun

Abstract—In this paper, a novel concept called simultaneously transmitting and reflecting RIS (STAR-RIS) is introduced into the wireless-powered mobile edge computing (MEC) systems to improve the efficiency of energy transfer and task offloading. Compared with traditional reflecting-only RIS, STAR-RIS extends the half-space coverage to full-space coverage by simultaneously transmitting and reflecting incident signals, and also provides new degrees-of-freedom (DoFs) for manipulating signal propagation. We aim to maximize the total computation rate of all users, where the energy transfer time, transmit power and CPU frequencies of users, and the configuration design of STAR-RIS are jointly optimized. Considering the characteristics of STAR-RIS, three operating protocols, namely energy splitting (ES), mode switching (MS), and time splitting (TS) are studied, respectively. For the ES protocol, based on the penalty method, successive convex approximation (SCA), and the linear search method, an iterative algorithm is proposed to solve the formulated non-convex problem. Then, the proposed algorithm for ES protocol is extended to solve the MS and TS problems. Simulation results illustrate that the STAR-RIS outperforms traditional reflecting/transmitting-only RIS. More importantly, the TS protocol can achieve the largest computation rate among the three operating protocols of STAR-RIS.

Index Terms—Wireless power transfer, mobile edge computing, reconfigurable intelligent surface, simultaneous transmission and reflection, resource allocation.

I. INTRODUCTION

The wireless communication and Internet of Things (IoT) have advanced at a remarkable pace in the past several years. It is envisioned that the number of IoT user equipments (UEs) will reach around 50 billion by 2030 [1]. These resource-limited UEs will generate a large amount of data traffic and require higher communication and computing capacities to meet their demands. As a promising technique, mobile edge computing (MEC) has been regarded as an alternative solution to lift the computing capability of UEs [2].

In the MEC systems, the servers are deployed in close proximity (e.g., access point) with UEs and UEs can offload partial or all computation tasks to MEC servers. In so doing, UEs’ task execution latency and energy consumption can be effectively reduced [3], [4]. Although the MEC can improve the computing performance of UEs, the energy of UEs is another bottleneck for system performance enhancement. Limited by their size, UEs can only store a finite amount of energy. To prevent the depletion of UEs’ battery power, the wireless power transfer (WPT) has been regarded as a thriving technology to provide stable and controllable energy supplies for UEs to prolong their lifetime [5]. By implementing the energy transmitter and energy harvesting modules on the access point (AP) and UEs respectively, UEs can harvest the energy transmitted by the AP, and then utilize the harvested energy to execute their computation tasks by local computing and task offloading [6].

Note that both the MEC and WPT are implemented by expanding the functions of the AP, which means these two techniques can be easily integrated to facilitate the wireless-powered MEC [7]. Such an integration brings many benefits for the system performance enhancement. For example, when the WPT is introduced into the MEC networks, the UEs can obtain stable energy supplies from the AP via the WPT to execute their tasks [8]. Meanwhile, thanks to the powerful computation capacity of the MEC server, the task processing time and energy consumption of UEs can be significantly reduced by offloading tasks to the MEC server. More importantly, with less task processing time, more time can be reserved for the UEs’ energy harvesting to prolong their lifetime [9].

However, when the wireless channels between the AP and UEs are blocked by some static or moving obstacles, the efficiency of the energy harvesting and task offloading in the wireless-powered MEC will be greatly reduced. Recently, an emerging paradigm called reconfigurable intelligent surface (RIS) has drawn great attentions due to its capability of smartly reconfiguring the wireless propagation environment [10]. The RIS is a man-made and metamaterial-based planar array consisting of a large number of reflecting elements. By dynamically adjusting the phase shift of each element through the smart controller attached to the RIS, the propagation of the wireless signals incident on the RIS can be controlled in a desirable way, such as enhancing the desired signals or...
By supporting both the electric and magnetic currents, each element of STAR-RIS can simultaneously reconfigure the transmitted and reflected signals, and thus achieve full-space coverage. Moreover, since both the transmission and reflection coefficient matrices can be designed, the STAR-RIS provides additional degrees-of-freedom (DoFs) to improve the channel conditions. Inspired by the benefits of STAR-RIS, we propose to introduce the STAR-RIS into the wireless-powered MEC. However, there are still some urgent challenges to be addressed before the STAR-RIS can be harmoniously integrated into the wireless-powered MEC. For example, although the phase shift problem for reflecting-only RIS has been intensively studied in various networks [15], [16], [17], the proposed algorithms cannot be directly applied to tackle the configuration problem of STAR-RIS. This is because there are three candidate operating protocols for STAR-RIS, namely energy splitting (ES), mode switching (MS), and time splitting (TS) [13]. The configuration of STAR-RIS needs to be designed according to different operating protocols. Meanwhile, apart from the phase shift, there are more adjustable parameters for the STAR-RIS, i.e., the amplitude adjustments for the ES/MS protocol, and the time allocation for the TS protocol. These parameters for the STAR-RIS are closely coupled with the communication and computing resource allocation for MEC as well as the energy transfer time for WPT, which results in a highly non-convex optimization problem. More importantly, despite the existing studies devoted to the optimization for different operating protocols of STAR-RIS in the downlink communications [13], [18], the proposed algorithms is not applicable to the UEs’ task offloading in the uplink. To be specific, when the ES/MS protocol is employed at the STAR-RIS for the MEC systems, the energy leakage, namely opposite-side leakage appears, where the UEs’ uplink offloading energy is wasted since only the transmitted/ reflected signals can be received by the AP [19]. If the TS protocol is applied by the STAR-RIS, the UEs located in the reflection/transmission space cannot offload task bits when the STAR-RIS operates in the transmission/reflection mode, which results in the reduction of offloading time. Since these operating protocols of STAR-RIS exhibit different features, it is of great importance to compare their performances in the wireless-powered MEC by designing appropriate optimization algorithms.

Motivated by these observations, we investigate the STAR-RIS-enhanced wireless-powered MEC systems in this paper to explore the potential benefits of STAR-RIS on the uplink task offloading and the downlink energy transfer. The main contributions of this paper are summarized as follows.

1) We propose a novel wireless-powered MEC system enhanced by the STAR-RIS, where the mission period is divided into the energy transfer stage and task offloading stage, and the STAR-RIS is deployed to assist the energy transfer in the downlink as well as the task offloading in the uplink. By considering the characteristics of STAR-RIS, the total computation rate maximization problems are formulated for all three operating protocols.

2) In the downlink energy transfer stage, the ES protocol is employed at the STAR-RIS and the coefficient matrices are optimized via a penalty method. Meanwhile, the energy transfer time for the ES/MS and TS protocols is optimized by a linear search method and the linear programming, respectively. In the uplink task offloading stage, the coefficient matrices optimization problems for three operating protocols of STAR-RIS are investigated separately, where an iterative algorithm is proposed to tackle the ES protocol and then the proposed algorithm is extended to solve the MS and TS protocols. Besides, the resource allocation of UEs, i.e., the transmit power and CPU frequency allocation, is optimized based on the successive convex approximation (SCA) technique.

3) Extensive simulation results unveil that for the three operating protocols of STAR-RIS, the computation rate first increases and then decreases with the growth of energy transfer time, while the energy transfer time that results in the maximum computation rate increases with larger mission period. Besides, the STAR-RIS exhibits a better performance than the conventional reflecting/transmitting-only RIS. More importantly, among the three protocols, the TS protocol can achieve the largest computation rate in the proposed system since the transmit power of UEs during the task offloading is able to be fully utilized by the AP and the interference among UEs can be greatly reduced compared to the ES and MS protocols.

The rest of the paper is organized as follows. Related works are discussed in Section II. In Section III, we introduce the system model and formulate the total computation rate maximization problems for all three operating protocols. Section IV elaborates on the proposed algorithms for solving the formulated problems. Some numerical results are shown in Section V, and conclusions are finally drawn in Section VI.

II. RELATED WORK

A. Wireless-Powered MEC

Recently, the MEC networks integrated with the WPT technique have been extensively investigated [20], [21], [22]. For example, in [20], following the binary offloading policy, a joint optimization algorithm based on the alternating direction method of multipliers (ADMM) decomposition technique is proposed to maximize the sum computation rate of all users in the wireless-powered MEC, where the users can execute their tasks via local computing or task offloading by utilizing the harvested energy. Differently, benefit from the partial offloading, in [22], the AP’s energy consumption for computing and WPT is minimized by optimizing the energy transmit beamforming at the AP, the CPU frequencies and the amount of offloaded bits at the users, as well as the time allocation. As expected, the proposed joint optimization algorithm can significantly reduce the energy consumption of the wireless-powered MEC systems.
However, it is worth noting that the linear energy harvesting model is applied in the above mentioned literature, which cannot properly model the power dependent energy harvesting efficiency. To tackle this problem, in [23], by adopting a practical non-linear energy harvesting model, F. Zhou et al. compare the performances of the partial offloading and the binary offloading in the wireless-powered MEC with the aim of maximizing the computation efficiency under the time division multiple access (TDMA) and the non-orthogonal multiple access (NOMA) protocols. Although simulation results verify that the partial offloading outperforms the binary offloading and NOMA outperforms TDMA in terms of computation efficiency, the randomness of task state information (TSI) and channel state information (CSI) is ignored. Therefore, in order to integrating the WPT into the MEC systems with dynamic task arrivals, Wang et al. [24] consider the TSI and the CSI with predicable and additive errors following arbitrary distribution, and then propose a sliding-window based online resource allocation design to minimize the total energy consumption for the wireless-powered MEC system, in which there is only one single AP that provides computing services and energy supplies for users. Thus, aiming to fully utilize the benefits brought by multiple APs, Wang et al. [7] propose a distributed algorithm to minimize the average task completion delay for the wireless-powered MEC networks with multiple edge servers, where both the simulation results and theoretical analysis demonstrate the advantages of the proposed algorithm in terms of the task completion delay and the convergence speed. The abovementioned literature illustrates the wireless-powered MEC is a promising technology to improve the computing capability and prolong the lifetime of UEs, but it still requires further investigation to accommodate unprecedented demands for high quality and ubiquitous wireless services.

B. RIS and STAR-RIS

Thanks to the favorable characteristics, RIS has received significant attentions from both the industry and academia. For instance, Mohjazi et al. [25] develop an analytical framework for the statistical analysis of the battery recharging time for the RIS-assisted WPT systems. Although this work provides some design insights for assessing the sustainability of RIS-assisted WPT systems, it only investigates the scenario that involves a single user. For multiple users, Yang et al. [26] aim to maximize the total received power by jointly optimizing the beamformer at transmitter and the phase-shifst at the RIS, where the user fairness is ensured by considering each users’ individual minimum received power constraints. Note that the data transmission is not considered in the above mentioned literature related to RIS-assisted WPT systems. In [27], Mao et al. deploy the RIS to assist the wireless-powered MEC, where the total computation bits maximization problem is tackled by an alternative optimization algorithm under the energy casualty constraints of IoT devices and RIS. From the simulation results, it can be seen that the proposed algorithm can achieve higher total computation bits compared to the scheme without RIS. Hu et al. [28] also introduce the WPT technology into the RIS-assisted secure systems and maximize the sum-rate under the imperfect CSI by an iterative algorithm. Since it pays attentions to the harvesting schedule at the RIS for supporting the energy consumption of RIS elements, the users cannot benefit from the integration of WPT and RIS.

Despite the attractive features of RIS, the geographical restrictions of transmitter and receiver impose difficulties on the practical implementation, which triggers the emergence of STAR-RIS [29], [30], [31], [32]. Nowadays, the investigation of STAR-RIS is still in its infancy. In [12], the concept of STAR-RIS is given, where a general hardware model and two channel models are proposed. Then, the candidate operating protocols of STAR-RIS are investigated in [13], which shows the advantages and disadvantages of three protocols of STAR-RIS. Afterwards, in [18] and [33], the comparison between orthogonal multiple access (OMA) and NOMA in the STAR-RIS-aided networks is discussed. Numerical results unveil that the integration of NOMA and STAR-RIS significantly outperforms networks employing conventional RIS and OMA. Furthermore, in [34], the STAR-RIS is employed to assist the UAV communication system, where the sum rate of all users is maximized by jointly optimizing the STAR-RIS’s beam-forming vectors, the UAV’s trajectory and power allocation. Simulations show that the STAR-RIS can achieve higher sum rate than traditional RIS, which verifies the superiority of the STAR-RIS technique. However, to the best of our knowledge, the integration of STAR-RIS and wireless-powered MEC has not yet been investigated in the existing literature.

III. SYSTEM MODEL AND PROBLEM FORMULATION

A. System Model

As shown in Fig. 1, we consider a STAR-RIS-enhanced wireless-powered MEC system, which consists of an AP, multiple UEs indexed by $i \in I \triangleq \{1, 2, \ldots, I\}$, and a STAR-RIS equipped with $M$ passive reflecting/transmitting elements indexed by $m \in M = \{1, 2, \ldots, M\}$. According to the location of STAR-RIS, the UE located in the transmission space is denoted by $t \in T$, while the UE located in the reflection space is denoted by $r \in R$. The numbers of UEs in the reflection and transmission spaces are $K_r$ and $K_t$, respectively, with $K_r + K_t = I$, and $R \cup T = I$. In our proposed system, the UEs are equipped with wireless energy-harvesting circuits, communication circuits and computing processors with limited computing capabilities. In addition, the UEs have computation tasks which involve a large amount of task-input data measured by bits. By utilizing the harvested energy, the UEs can execute their task-input data through local computing and task offloading. The AP is endowed with a high performance MEC server to help UEs compute their task-input data. Besides, an RF energy transmitter is also embedded in the AP to provide energy supplies for UEs with the aid of WPT. The STAR-RIS which can simultaneously transmit and reflect the incident signal is deployed to assist the UEs’ task offloading and the AP’s energy transfer.

1) Channel Model: Similar to [13], [33], it is assumed that the direct communication links between the AP and the UEs are blocked by obstacles. The downlink channel coefficients from the AP to the STAR-RIS, and from the
STAR-RIS to the $i$-th UE are expressed as $\mathbf{g}_\text{RIS}^{\text{AP}} \in \mathbb{C}^{1 \times M}$ and $\mathbf{g}_\text{RIS} \in \mathbb{C}^{1 \times M}$, respectively. The counterpart uplink channel coefficients are given by $\mathbf{h}_\text{RIS}^{\text{AP}} \in \mathbb{C}^{M \times 1}$ and $\mathbf{h}_\text{RIS} \in \mathbb{C}^{1 \times M}$. Besides, we suppose that the perfect channel state information of all channels is available at the AP through the advanced channel estimation technologies.\(^1\)

Different from the conventional RIS with non-magnetic elements, by introducing the equivalent surface electric and magnetic currents into the model, the transmitted and reflected signals can be equivalently treated as waves radiated from the time-varying surface equivalent electric currents and magnetic currents. Then, by adjusting the transmission and reflection coefficients which are related to the surface impedances, both the transmitted and reflected signals can be reconfigured to realize the full-space coverage. There are three protocols for operating the STAR-RIS in the wireless-powered MEC, i.e., ES, MS, and TS [13], [31]. To be more specific, for the ES protocol during the task offloading, all elements work in the simultaneous transmission and reflection mode. Denoting the amplitude adjustments of the $m$-th element for reflection and transmission as $\beta_{m,r}$ and $\beta_{m,t}$, we have $\sum_{m} \beta_{m,r} + \sum_{m} \beta_{m,t} = 1$ with $\beta_{m,r}, \beta_{m,t} \in [0,1]$. Note that for the ES protocol, the incident signals from UEs are divided into reflected and transmitted signals by the STAR-RIS, the ES protocol, and the AP can only receive the transmitted or reflected signals. Thus, the uplink offloading energy for UEs located in the transmission/reflection space will be leaked to the reflection/transmission side, i.e., the opposite-side leakage appears, which results in the waste of UEs’ offloading energy. Besides, the phase shifts of the $m$-th element for reflection and transmission can be given by $\theta_{m,r}$ and $\theta_{m,t}$, with $\theta_{m,r}, \theta_{m,t} \in [0,2\pi)$. Thus, the reflection- and transmission-coefficient matrices of the STAR-RIS can be given by $\mathbf{u}_r^{\text{ES}} = \text{diag} \left( \beta_{1,r} e^{j\theta_{1,r}}, \ldots, \beta_{M,r} e^{j\theta_{M,r}} \right)$ and $\mathbf{u}_t^{\text{ES}} = \text{diag} \left( \beta_{1,t} e^{j\theta_{1,t}}, \ldots, \beta_{M,t} e^{j\theta_{M,t}} \right)$.

For the MS protocol, each element of the STAR-RIS can be operated either in reflection mode or transmission mode. Thus, there are binary constraints for the amplitude adjustments, i.e., $\beta_{m,r} + \beta_{m,t} = 1$ with $\beta_{m,r}, \beta_{m,t} \in \{0,1\}$. Similar to the ES protocol, the coefficient matrices of MS protocol for STAR-RIS during the task offloading can be expressed as $\mathbf{u}_r^{\text{MS}} = \text{diag} \left( \beta_{1,r} e^{j\theta_{1,r}}, \ldots, \beta_{M,r} e^{j\theta_{M,r}} \right)$ and $\mathbf{u}_t^{\text{MS}} = \text{diag} \left( \beta_{1,t} e^{j\theta_{1,t}}, \ldots, \beta_{M,t} e^{j\theta_{M,t}} \right)$.

For the TS protocol, all elements of the STAR-RIS work in the same mode (i.e., reflection or transmission mode). Denote the reflection time and transmission time as $\tau_r$ and $\tau_t$, respectively. By optimizing $\tau_r$ and $\tau_t$, the STAR-RIS can sequentially switch all elements of STAR-RIS to assist the task offloading of UEs that are located in the reflection and transmission spaces, and hence achieve full-space coverage. Nevertheless, it can be found that the UEs located in the reflection/transmission space cannot offload task bits when the STAR-RIS operates in the transmission/reflection mode, which results in the reduction of offloading time of UEs. The coefficient matrices of TS protocol for reflection and transmission modes are given by $\mathbf{u}_r^{\text{TS}} = \text{diag} \left( e^{j\theta_{1,r}}, \ldots, e^{j\theta_{M,r}} \right)$ and $\mathbf{u}_t^{\text{TS}} = \text{diag} \left( e^{j\theta_{1,t}}, \ldots, e^{j\theta_{M,t}} \right)$.

With the coefficient matrices of STAR-RIS, the combined uplink channel between UE $i$ and the AP can be expressed as $h_i^{\text{U}} = h_i^{\text{RIS}} X h_i^{\text{AP}}$, where $k \in \{r,t\}$ represents the operating mode and $X \in \{\text{ES, MS, TS}\}$ indicates the employed STAR-RIS operating protocol. If UE $i$ is located in the reflection space, $k = r$. Otherwise, $k = t$.

2) Energy Transfer and Task Offloading: As illustrated in Fig. 2, the mission period $T$ is divided into three stages, i.e., the downlink energy transfer stage, the uplink task offloading stage, and the edge computing and result downloading stage. Specifically, in the first stage, the time allocated to the energy transfer is $\tau_0$. In order to ensure all UEs in the transmission and reflection spaces can fairly harvest energy, we suppose that the ES protocol is employed at the STAR-RIS for the WPT. Moreover, the process of energy transfer can be regarded as a special multicast transmission. In this case, the ES protocol is appealing since it can make full use of the entire available communication time.
and allows the UEs to harvest energy all through the first stage [13]. Thus, the coefficient matrices of STAR-RIS in the downlink energy transfer can be given by \( \mathbf{u}_{i,\text{ES}}^D = \text{diag} \left( \sqrt{\beta_{1,i}^D} e^{j\theta_{1,i}}, \sqrt{\beta_{2,i}^D} e^{j\theta_{2,i}}, \ldots, \sqrt{\beta_{M,i}^D} e^{j\theta_{M,i}} \right) \) and \( \mathbf{u}_{i,\text{TS}}^D = \text{diag} \left( \sqrt{\beta_{1,i}^D} e^{j\theta_{1,i}}, \sqrt{\beta_{2,i}^D} e^{j\theta_{2,i}}, \ldots, \sqrt{\beta_{M,i}^D} e^{j\theta_{M,i}} \right) \). Similarly, the combined downlink channel between UE \( i \) and the AP can be given by \( h_{i,k}^D = g_{i,k}^U \mathbf{u}_{i,\text{ES/TS}}^D R \), \( k \in \{ r, t \} \).

During the energy transfer stage, the transmit power of the AP is denoted as \( P_0 \). According to the non-linear energy harvesting model \([28],[37]\), the harvested energy of UE \( i \) can be expressed as
\[
E_{i,\text{har}}^i (\tau_0, |h_i^D|^2) = \frac{\tau_0 \xi_i}{1 + \exp (-a_i (P_0 |h_i^D|^2 - b_i))} - \frac{\tau_0 \psi_i}{\exp (a_i b_i)},
\]
where \( \xi_i = \psi_i (1 + \exp (a_i b_i)) / \exp (a_i b_i) \). \( a_i \) and \( b_i \) are constants of UE \( i \) related to the detailed circuit specifications such as the resistance, capacitance, and diode turn-on voltage. \( \psi_i \) represents the maximum harvested power at UE \( i \) when the circuit is saturated.

In the task offloading stage, the power-domain NOMA is applied and the system bandwidth is denoted as \( B \). Since the size of computing result is often trivial compared with that of the original tasks and the computing capacity of MEC server is ultra-high, the time for edge computing and result downloading can be ignored \([27]\). Thus, the offloading time of UEs for the ES/MS protocol can be given by \( T - \tau_0 \). While for the TS protocol, the offloading time of UE \( i \) can be expressed as
\[
\tau_{i,k} = \begin{cases} \tau_r \text{, if UE } i \text{ is located in the reflection space;} \\ \tau_t \text{, if UE } i \text{ is located in the transmission space.} \end{cases}
\]
Then, denoting the transmit power of UE \( i \) and the noise power as \( p_i \) and \( \sigma^2 \), respectively, the amount of offloading task bits of UE \( i \) for the ES/MS protocol can be expressed as
\[
L_{\text{ES/MS},i}^{\text{off}} = (T - \tau_0) B \log \left( 1 + \frac{p_i |h_i^U|^2}{\sum_{j \neq i} p_j |h_j^U|^2 + \sigma^2} \right).
\]
Correspondingly, if the TS protocol is employed at the STAR-RIS, the amount of offloading task bits of UE \( i \) can be given by \(^2\)
\[
L_{\text{TS},i}^{\text{off}} = \tau_{i,k} B \log \left( 1 + \frac{p_i |h_i^U|^2}{\sum_{j \neq i} p_j |h_j^U|^2 + \sigma^2} \right).
\]

3) Energy Consumption Model: Benefiting from the partial offloading scheme, the UEs’ task-input bits can be arbitrarily divided to facilitate parallel computing at UEs and at the AP. Therefore, the energy consumption of UEs consists of the energy consumed by task offloading and local computing. Since the offloading time is different for ES/MS and TS protocols, the offloading energy consumption of UE \( i \) in ES/MS can be given by \( p_i (T - \tau_0) \). While for TS, the offloading energy consumption of UE \( i \) can be expressed as \( p_i \tau_{i,k} \).

For the local computing, the dynamic voltage and frequency scaling (DVFS) model is adopted to express the UEs’ energy consumption \([38],[39]\). Denote the CPU frequency of UE \( i \) as \( f_i \). Hence, the energy consumption of UE \( i \) for local computing can be given by
\[
E_{i,\text{loc}}^i = \kappa (T - \tau_0) f_i^3,
\]
where \( \kappa \) is the effective capacitance coefficient that depends on the processor’s chip architecture.

In addition, the amount of task bits that is computed locally at UE \( i \) can be given by
\[
L_{i,\text{loc}} = f_i (T - \tau_0),
\]
where \( C_i \) is the CPU cycles required for computing 1-bit of task-input data.

B. Problem Formulation

In this paper, we aim to maximize the total computation rate of all UEs in the STAR-RIS-enhanced wireless-powered MEC system by jointly optimizing the energy transfer time, transmit power and CPU frequencies of UEs, and the configuration design of the STAR-RIS. Based on the characteristics of STAR-RIS, the computation rate maximization problems are formulated for all three operating protocols.

1) Problem Formulation for ES/MS Protocol: The computation rate maximization problems for the ES/MS protocol can be formulated as
\[
\max_{\mathbf{z}} \sum_{i=1}^{I} \left( L_{\text{loc}}^{i} + L_{\text{ES/MS},i}^{\text{off}} \right)
\]
subject to
\[
\begin{align}
& f_i \leq F_{\text{max}}, \forall i \in I, \\
& p_i \leq P_{\text{max}}, \forall i \in I, \\
& \tau_0 \leq T, \\
& \| \theta_{m,t}^n \| = 1, \forall m \in M, k \in \{ r, t \}, n \in \{ D, U \}, \\
& \beta_{m,t}^r + \beta_{m,r}^r = 1, \forall m \in M, n \in \{ D, U \}, \\
& 0 \leq \beta_{m,t}^r, \beta_{m,r}^r \leq 1, \forall m \in M, n \in \{ D, U \}, \\
& \beta_{m,t}^U, \beta_{m,r}^U \in \{ 0, 1 \}, \forall m \in M \text{(only valid for MS)},
\end{align}
\]
where \( \mathbf{z} = \{ \tau_0, f_i, p_i, \mathbf{u}_{i,\text{ES}}^D, \mathbf{u}_{i,\text{ES/TS}}^D \} \). \( F_{\text{max}} \) and \( P_{\text{max}} \) are the UEs’ maximum transmit power and CPU frequency, respectively. Constraint (7b) represents the energy consumption of UE \( i \) should be less than the harvested energy from the AP. Constraints (7f) is the feasible set of STAR-RIS’s phase shift. (7g) and (7h) are the energy conservation constraints of STAR-RIS. (7i) indicates the binary constraint for each element of STAR-RIS and it is only valid for MS protocol. Note that for the ES protocol, when \( \beta_{m,t}^U, \beta_{m,r}^U \in \{ 0, 1 \} \), it is

\(^2\)Note that the beamforming is not considered in the uplink since each UE is equipped with one single antenna. When the UEs are implemented by the antenna arrays, each antenna’s transmit power can be successively optimized by our solution. More sophisticated uplink beamforming design for the MIMO systems is an interesting topic for our future work.
obtained by optimizing transfer time $\tau_0$ and the coefficient matrices of STAR-RIS $\{\mathbf{u}_{k,\text{ES}}, \mathbf{u}_{k,\text{TS}}\}$ are given, problem (7) with ES protocol can be reformulated as

$$
\max_{p_i, f_i} \sum_{k=1}^{K} \left( L^{\text{loc}}_{t_i} + L^{\text{off}}_{\text{ES},k} \right) \quad \text{(9a)}
$$

subject to

$$
\left\{ \right.
\begin{array}{l}
(7b) - (7d).
\end{array}
$$

To tackle the non-convex objective function in (9), we first define $R_i = \log \left( \sum_{j \neq i} p_j |h_{ij}^U|^2 + \sigma^2 \right)$ and thus $L^{\text{off}}_{\text{ES},k}$ can be written as

$$
L^{\text{off}}_{\text{ES},k} = (T - \tau_0) B \left( \log \left( \sum_{i=1}^{I} p_i |h_{ij}^U|^2 + \sigma^2 \right) - R_i \right) \quad \text{(10)}
$$

By taking the first-order Taylor expansion of $R_i$ with respect to $p_j$, we have

$$
R_i \leq \log \left( \sum_{j \neq i} p_j^{(l)} |h_{ij}^U|^2 + \sigma^2 \right)
$$

$$
+ \sum_{j \neq i} \frac{|h_{ij}^U|^2}{\ln 2} \left( \sum_{j \neq i} p_j^{(l)} |h_{ij}^U|^2 + \sigma^2 \right) (p_j - p_j^{(l)}) = \tilde{R}_i,
$$

where $p_j^{(l)}$ is the transmit power of UE $j$ at the $l$-th iteration. Then, by replacing $R_i$ in (10) with $\tilde{R}_i$, during the $l$-th iteration, problem (9) can be approximated as

$$
\max_{p_i, f_i} \sum_{i=1}^{I} \left( T - \tau_0 \right) B \left( \log \left( \sum_{i=1}^{I} p_i |h_{ij}^U|^2 + \sigma^2 \right) - \tilde{R}_i \right)
$$

$$
+ \sum_{i=1}^{I} f_i (T - \tau_0) C_i \quad \text{(12a)}
$$

subject to

$$
(7b) - (7d). \quad \text{(12b)}
$$

We find that the objective function of (12) is concave with respect to $f_i$ and $p_i$. Besides, constraint (7b) is convex, and (7c) as well as (7d) are linear. Thus, problem (12) is a convex optimization problem, which can be solved efficiently by standard solvers, such as the CVX [40]. Then, based on the SCA technique, by iteratively updating $p_i$ and $f_i$ via solving the convex problem (12) until convergence, the solution to problem (9) can be obtained. Thus, the resource allocation algorithm for solving problem (9) with ES protocol can be summarized as Algorithm 1.

2) Coefficient Matrices Optimization for STAR-RIS: With given $\tau_0, p_i$, and $f_i$, problem (7) with ES protocol can be transformed into

$$
\max_{\mathbf{u}_{k,\text{ES}}, \mathbf{u}_{k,\text{TS}}} \sum_{i=1}^{I} L^{\text{off}}_{\text{ES},i} \quad \text{(13a)}
$$

subject to

$$
(7b), (7f) - (7h). \quad \text{(13b)}
$$

It can be observed that problem (13) is non-convex and challenging to be solved directly. In order to transform it into a more tractable form, we first define $\mathbf{h}_i = \text{diag} (\mathbf{h}_{ij}^{\text{RIS}}) \mathbf{h}_{ij}^{\text{AP}} \in \mathbb{C}^{M \times 1}$.
Thus, the uplink channel gain between UE $i$ and AP can be expressed as $|h_i|^2 = |h_i^RIS| = |h_i^{AP}|^2 = \text{Tr}(V_i^H H_i)$. Similarly, in the downlink, $|h_i|^2 = |g_i^RIS| = |g_i^{AP}|^2 = \text{Tr}(V_i^H G_i)$, where $V_i^D = u_i^D_{ES}^H u_i^D_{ES}^H H_i \in \mathbb{C}^{M \times M}$, $G_i = g_i^H h_i^L$, and $g_i = \text{diag}(g_i^{RIS}) g_i^{AP} \in \mathbb{C}^{M \times M}$.

Theorem 1: When the optimal solution to problem (13) with ES protocol is obtained, constraint (7b) must hold with equality, i.e.,
\[
\kappa (T - \tau_0) f_i^3 + p_i (T - \tau_0) = E_{\text{har}}^i (\tau_0, \text{Tr}(V_i^D H_i)).
\]

Proof: The theorem can be proved by contradiction. Assume that the optimal solution to problem (13) with ES protocol is $\{\tau_0^*, f_i^*, p_i^*, u_i^D_{ES}^*, u_i^U_{ES}^*, s_i^*, f_i^D, s_i^D, \}$. If $\kappa (T - \tau_0) f_i^3 + p_i (T - \tau_0) < E_{\text{har}}^i (\tau_0, \text{Tr}(V_i^D H_i))$, then the following actions can be taken: 1) reduce the energy transfer time $\tau_0^*$, and/or 2) increase the local computing frequency $f_i^D$, and/or 3) increase the transmit power $p_i^*$ without violating the other constraints, to further increase the computation rate. Therefore, the assumed optimal solution is not optimal. Thus, the conclusion in Theorem 1 is proved.

According to Theorem 1, the penalty method can be applied to ensure the equality of (7b) and optimize the downlink coefficient matrices of STAR-RIS. To this end, constraint (7b) is transformed into a penalty term added to the objective function. Thus, problem (13) can be transformed into
\[
\max_{u_i^D_{ES}, u_i^U_{ES}} \sum_{i=1}^I (T - \tau_0) B \log(1 + \frac{p_i \text{Tr}(V_i^D H_i)}{\gamma (V_k^t, V_k^r)^f} + \mu \kappa (T - \tau_0) f_i^3 + p_i (T - \tau_0) - E_{\text{har}}^i (\tau_0, \text{Tr}(V_i^D H_i)))
\]
\[
\text{s.t. rank}(V_k^n) = 1, n \in \{D, U\}, k \in \{r, t\}, (Tf) - (7h)_i
\]
where $\mu$ is the penalty factor. $\mu$ is chosen as a large positive constant, which can force the penalty term to be equal to zero and then obtain the optimal downlink coefficient matrices of STAR-RIS.

Problem (15) is still non-convex due to the objective function and constraint (15b). To tackle the non-convex objective function of (15), the auxiliary variables $A_i$, $B_i$, and $z_i$ are introduced, with $1/A_i \leq \text{Tr}(V_k^n H_i) p_i$, $B_i \geq \sum_{j \neq i} \text{Tr}(V_k^t H_j) p_j + \sigma^2$, and $z_i \geq \exp (-a_i (p_j \text{Tr}(V_k^D H_i) - b_i))$. Then, the objective function of problem (15) can be written as
\[
\sum_{i=1}^I (T - \tau_0) B \log(1 + \frac{1}{A_i}) + \sum_{i=1}^I \mu \kappa (T - \tau_0) f_i^3 + \sum_{i=1}^I \mu (p_i (T - \tau_0) - \tau_0 (\frac{\xi_i - \psi_i}{1 + z_i} + \frac{z_i - z_i^0}{1 + z_i^{0}}))
\]

By taking the first-order Taylor expansion of $\log(1 + 1/A_i)$ with respect to $A_i$ and $B_i$, we have
\[
\log(1 + \frac{1}{A_i}) = \log(1 + \frac{1}{A_i^{(0)}} B_i^{(0)}) - \frac{(\log(e))(A_i - A_i^{(0)})}{A_i^{(0)}} - \frac{(\log(e))(B_i - B_i^{(0)})}{B_i^{(0)}} = \tilde{R}_i,
\]
where $A_i^{(0)}$ and $B_i^{(0)}$ are local points of $A_i$ and $B_i$ at the $l$-th iteration. For the term $1/(1 + z_i)$, by executing the same transformation, we have
\[
\frac{1}{1 + z_i} \geq \frac{1}{1 + z_i^0} - \frac{1}{1 + z_i^{0}} \frac{z_i - z_i^0}{(1 + z_i^0)^2}
\]

Thus, the non-convex objective function of (15) can be approximated as
\[
\sum_{i=1}^I (T - \tau_0) B \tilde{R}_i + \sum_{i=1}^I \mu \kappa (T - \tau_0) f_i^3 + p_i (T - \tau_0) - \tau_0 (\frac{\xi_i - \psi_i}{1 + z_i})
\]

Theorem 2: The constraint (15b), i.e., $\text{rank}(V_k^n) = 1$, can be approximated by $\text{Tr}(V_k^n) - \gamma (V_k^n, V_k^n)^f \leq \varepsilon$, where $\gamma (V_k^n, V_k^n)^f = \|V_k^n\|_{s} + \left(\|V_k^n - (V_k^n)^f\|_{s} \right)$, $\partial V_k^n \|V_k^n\|_{s}$ and $\varepsilon$ is a positive threshold.

Proof: Denote the $m$-th largest singular value of $V_k^n$ as $\rho_m (V_k^n)$. Thus, we have $\text{Tr}(V_k^n) = \sum_{m=1}^M \rho_m (V_k^n)$ and $\|V_k^n\|_{s} = \rho_1 (V_k^n)$, where $\|V_k^n\|_{s}$ represents the spectral norm of $V_k^n$. When the rank-one constraint is satisfied with $\rho_1 (V_k^n) > 0$ and $\rho_m (V_k^n) = 0, m \neq 1$, the rank-one constraint can be transformed into
\[
\text{Tr}(V_k^n) - \|V_k^n\|_{s} = 0.
\]

At the $l$-th iteration, a lower-bound of $\|V_k^n\|_{s}$ can be given by
\[
\gamma (V_k^n, (V_k^n)^f) = \|V_k^n\|_{s} + \left(\|V_k^n - (V_k^n)^f\|_{s} \right)
\]

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Algorithm 2 The SCA-Based Algorithm for Solving Problem (13) With ES Protocol

1. Initialize $u_{k,ES}^{P(0)}, u_{k,ES}^{U(0)}, A_t^{(0)}, B_t^{(0)}$, and $z_t^{(0)}$, and set the iterative number $l = 0$;
2. while $\sum_{i=1}^{L} L_{ES,i}^{\text{off}} ((i+1) - \sum_{i=1}^{L} L_{ES,i}^{\text{off}} (l)) \geq \varepsilon$ do
3. Calculate $\hat{R}_t^{(l)}, \hat{Z}_t^{(l)}$, and $\gamma(V_k^{(l)}(V_k^{(l)}))$ based on (17), (18), and (21), respectively;
4. Solve the convex optimization problem (22) to obtain $u_{k,ES}^{P(l+1)}, u_{k,ES}^{U(l+1)}, A_t^{(l+1)}$, $B_t^{(l+1)}$, and $z_t^{(l+1)}$;
5. Update the iterative index $l = l + 1$;
6. end while

Thus, (15b) can be approximated by $\text{Tr}(V_k^n) - \gamma(V_k^{(n)}(V_k^{(n)})) \leq \varepsilon$. Theorem 2 is proved.

Based on Theorem 2, the rank one constraint (15b) can be tackled by its approximated form [16], [28]. Thus, problem (15) is reformulated as

$$
\begin{align*}
\max_{u_{k,ES}^{P}, u_{k,ES}^{U}, A_t, B_t, z_t} & \sum_{i=1}^{L} (T - \tau_0) B \hat{R}_t \\
\text{s.t.} & \frac{1}{A_t} \leq \text{Tr}(V_k^{U} H_i)p_i, k \in \{r, t\}, \forall i, I, \\
& B_t \geq \sum_{j \neq t} \text{Tr}(V_k^{U} H_j)p_j + \sigma^2, k \in \{r, t\}, \forall i, I, \\
& z_t \geq \exp \left(-a_t (P_t \text{Tr}(V_k^{D} H_i) - b_t)\right), k \in \{r, t\}, \forall i, I, \\
& \text{Tr}(V_k^{n}) - \gamma(V_k^{(n)}(V_k^{(n)})) \leq \varepsilon, n \in \{D, U\}, k \in \{r, t\}.
\end{align*}
$$

Algorithm 3 Proposed Algorithm to Solve Problem (7) for ES With Specific Energy Transfer Time $\tau_0$

1. Initialize $p_i^{(0)}, f_i^{(0)}, u_{k,ES}^{P(0)}, u_{k,ES}^{U(0)}$, and set the iterative number $t = 1$;
2. repeat:
3. Solve the resource allocation problem (9) to obtain $p_t^{(t)}$ and $f_t^{(t)}$ by Algorithm 1;
4. Denote the objective function of (7) as $L_{ES}^{\text{sum}}(t)$;
5. Update the iterative index $t = t + 1$;
6. until $t > N_{\text{max}}$ or $|L_{ES}^{\text{sum}}(t+1) - L_{ES}^{\text{sum}}(t)| \leq \delta$;
7. Output the resource allocation and coefficient matrices optimization result $\{p_i^{*}, f_i^{*}, u_{k,ES}^{P*}, u_{k,ES}^{U*}\}$

Algorithm 4 Joint Resource Allocation and Coefficient Matrices Optimization Algorithm for ES Protocol

1. Initialize the step size $\Delta$ as a small number and $\tau_0 = 0$;
2. while $\tau_0 \leq T$ do:
3. Run Algorithm 3 to obtain $p_t^{*}, f_t^{*}, u_{k,ES}^{P*}$ and $u_{k,ES}^{U*}$;
4. Denote the objective function of (7) as $L_{ES}^{\text{sum}}(\tau_0)$;
5. Update $\tau_0 = \tau_0 + \Delta$;
6. end while;
7. Output $\tau_0 = \arg \max_{\tau_0} L_{ES}^{\text{sum}}(\tau_0)$ and the corresponding resource allocation and coefficient matrices optimization result $\{p_i^{*}, f_i^{*}, u_{k,ES}^{P*}, u_{k,ES}^{U*}\}$ for problem (7) with ES protocol.

It can be found that problem (22) is a standard convex semidefinite program (SDP) and can be solved via classical convex optimization toolboxes, such as the SDP solver in CVX [41]. By iteratively updating $A_t, B_t, z_t$ and $V_k^n$ via solving the convex problem (22) until convergence, the solution to problem (13) can be achieved and the coefficient matrices of STAR–RIS in both uplink and downlink can be obtained. The proposed SCA-based algorithm for solving problem (13) can be summarized as Algorithm 2.

For the given energy transfer time $\tau_0$, the proposed algorithm to solve problem (7) with ES protocol can be outlined in Algorithm 3. The initial point of Algorithm 3 can be found by observations. For example, we can set $p_i^{(0)} = 0$, $f_i^{(0)} = 0$, $\theta_m^{(0)} = 0$, and $\beta_m^{(0)} = 0.5$, which satisfy all constraints in problem (7) for the ES protocol.

Remark 2: Since problem (7) with ES protocol only involves a single continuous variable $\tau_0$, the linear search method can be used to obtain the optimal energy transfer time $\tau_0$ [31], [42]. To be specific, within the interval $(0, T)$, $\tau_0$ is updated with a small step size $\Delta$. With given $\tau_0$, we solve the total computation rate maximization problems with ES protocol by Algorithm 3 and obtain $\{p_i^{*}, f_i^{*}, u_{k,ES}^{P*}, u_{k,ES}^{U*}\}$. By examining all the discrete values of $\tau_0$, the maximum computation rate and the optimal solution for problem (7) with ES protocol can be obtained with desired accuracy.

Based on Remark 2, the proposed joint resource allocation and coefficient matrices optimization algorithm for solving problem (7) with ES protocol is outlined in Algorithm 4.

B. Solution to the MS Protocol

Compared to the ES protocol, problem (7) with the MS protocol is a mixed-integer non-convex optimization problem due to the binary constraint (7i). To tackle this problem, the binary constraint is equivalently transformed into an equality, i.e.,

$$\beta_{m,k}^U (\beta_{m,k}^U - 1) = 0.\quad (23)$$

By further adding the equality constraint (23) as another penalty term into the objective function, problem (7) with MS

1Note that the complexity of proposed algorithm will be affected by $\Delta$. In our future work, we would like to design a linear search method with adaptive step size to further reduce the computational complexity.
protocol can be transformed into
\[
\max_\mathbf{x} \sum_{i=1}^{I} \left( L_{i, \text{loc}} + L_{i, \text{MS}, i} \right) + \sum_{m=1}^{M} \sum_{k \in \{r, t\}} \nu \left( \beta_{m,k}^U \left( \beta_{m,k}^U - 1 \right) \right)
\]
\[\text{s.t.} \ (7b) - (7g), \tag{24a}\]
where \( \nu \) is a positive penalty factor. Similar to the method for ES protocol, with given \( \tau_0 \), the problem is decomposed into two subproblems, namely, the resource allocation of UEs and the coefficient matrices optimization for STAR-RIS with the MS protocol. To be more specific, for the subproblem of resource allocation of UEs, it can be solved by a similar method to the ES protocol. While for the subproblem of coefficient matrices optimization for MS protocol, since the penalty term about \( \beta_{m,k}^U \) renders the objective function non-convex, the Taylor expansion is exploited again to obtain the lower convex bound of the penalty term at the \( t \)-th iteration, i.e.,
\[
\beta_{m,k}^U \left( \beta_{m,k}^U - 1 \right) \geq \left( 2 \beta_{m,k}^U - 1 \right) \beta_{m,k}^U \left( \beta_{m,k}^U \right)^2. \tag{25}\]
Thus, the subproblem of coefficient matrices optimization for MS protocol during the \( t \)-th iteration can be reformulated as
\[
\max_{U_{k,\text{MS}}, U_{k,\text{ES}}} \frac{1}{I} \sum_{i=1}^{I} \left( T - \tau_0 \right) B \dot{R}_{i} + \sum_{i=1}^{I} \left( T - \tau_0 \right) \left( \xi_i \frac{\psi_i}{\exp \left( a_i b_i \right)} \right)
\]
\[\text{s.t.} \ (22b) - (22e). \tag{26a}\]
which is a standard convex problem.

By iteratively solving the subproblems of UEs’ resource allocation and the coefficient matrices optimization for STAR-RIS with MS protocol, the computation rate maximization problem with given energy transfer time \( \tau_0 \) can be handled effectively. Then, by exploiting the linear search method, the optimal energy transfer time \( \tau_0^* \) and the corresponding solution to problem (7) with MS protocol can be finally obtained. The proposed algorithm for solving problem (7) with MS protocol is outlined in Algorithm 5.

### C. Solution to the TS Protocol

To solve the total computation rate maximization problem for the TS protocol, problem (8) is decomposed into three subproblems, i.e., the time allocation, the resource allocation of UEs, and the coefficient matrices optimization for STAR-RIS.

**Remark 3:** When the TS protocol is employed at the STAR-RIS during the task offloading, all elements work either in the transmission mode or the reflection mode depending on the transmission and reflection time allocation. Specifically, when the elements of STAR-RIS work in the transmission mode, \( \beta_{m,t}^U = 1, \beta_{m,r}^U = 0 \). Otherwise, \( \beta_{m,t}^U = 0, \beta_{m,r}^U = 1 \).

**Algorithm 5 Proposed Algorithm to Solve Problem (7) With MS Protocol**

1. Initialize the variables \( p_i(0), f_i(0), u_{k,\text{ES}}^D(0), u_{k,\text{MS}}^U(0) \), the small step \( \Delta \), and set \( \tau_0 = 0 \);
2. **repeat:** Outer loop
   3. Set the energy transfer time \( \tau_0 = \tau_0 + \Delta \) and the iteration number \( t = 0 \);
   4. **repeat:** Inner loop
      5. Solve the resource allocation problem for MS to obtain \( p_i(t) \) and \( f_i(t) \);
      6. Solve the coefficient matrices optimization problem for MS to obtain \( u_{k,\text{ES}}^D(t) \) and \( u_{k,\text{MS}}^U(t) \);
      7. Calculate \( L_{\text{sum}}^M(t) = \sum_{i=1}^{I} \left( L_{i, \text{loc}} + L_{i, \text{MS}, i} \right) \);
      8. Update the iterative index \( t = t + 1 \);
   9. **Until** \( t > N_{\text{max}} \) or \( L_{\text{sum}}^M(t + 1) - L_{\text{sum}}^M(t) \) \( \leq \delta \);
10. Update \( L(\tau_0) = L_{\text{sum}}(t + 1) \);
11. **Until** \( \tau_0 > T_r \);  
12. **Output:** \( \tau_0^* = \arg \max_{\tau_0} L(\tau_0) \) and the corresponding solution to resource allocation and coefficient matrices optimization \( \{ p_i^*, f_i^*, u_{k,\text{ES}}^D, u_{k,\text{MS}}^U \} \).

Thus, there is no need to optimize \( \beta_{m,k}^U \) for the TS protocol. Nevertheless, the time allocation for the TS protocol is more complex compared with the ES/MS protocol, since the time allocated to the energy transfer, the reflection and transmission modes need to be jointly considered. To overcome this difficulty, we first define (27), as shown at the bottom of the next page.

\[
C = \begin{bmatrix}
-\kappa f_i^3 & -\eta P_0 \left| h_D^2 \right|^2 & 0 & 0 \\
-\kappa f_i^3 & -\eta P_0 \left| h_D^2 \right|^2 & 0 & p_t \\
1 & 1 & 1 & 1 \\
\end{bmatrix}, \tag{28}
\]
\[
D = \begin{bmatrix}
-\kappa T_r^3 & -\kappa T_i^3 \\
T_r & T_i \\
\end{bmatrix}^H. \tag{29}
\]

Therefore, for problem (8), when the results for resource allocation of UEs \( \{ p_i, f_i \} \) and the coefficient matrices optimization of STAR-RIS \( \{ u_{k,\text{ES}}^D, u_{k,\text{TS}}^U \} \) are given, the time allocation problem for the TS protocol can be expressed as
\[
\max_{\Lambda} \Lambda L \tag{30a}
\]
\[\text{s.t.} \ A \Lambda \leq D, \tag{30b}\]
\[\Lambda \geq 0, \tag{30c}\]
where \( \Lambda = [\tau_0 \ \tau_r \ \tau_i]^H \). (30) is a standard linear programming (LP) problem and can be easily solved.

Then, with given time allocation \( \Lambda \) and the coefficient matrices of STAR-RIS \( \{ u_{k,\text{ES}}^D, u_{k,\text{MS}}^U \} \), the subproblem of UEs’ resource allocation for the TS protocol can be formulated as
\[
\max_{p_i,f_i} \sum_{i=1}^{I} \left( L_{i, \text{loc}} + L_{i, \text{TS}, i} \right) \tag{31a}
\]
\[\text{s.t.} \ (8b) - (8d). \tag{31b}\]
Algorithm 6 Proposed Algorithm for Solving Problem (8) With TS Protocol

1. Initialize the vector $\mathbf{A}^{(0)}, p_i^{(0)}, f_i^{(0)}, \mathbf{u}_i^{D,(0)}, \mathbf{u}_i^{U,(0)}$ and set the iteration number $t = 0$;
2. repeat:
3. Solve the LP problem (30) for TS to obtain the time allocation $\mathbf{A}^{(t)}$;
4. Solve the resource allocation problem for TS to obtain $p_i^{(t)}$ and $f_i^{(t)}$;
5. Solve the coefficient matrices optimization problem for TS to obtain $\mathbf{u}_i^{D,(t)}$ and $\mathbf{u}_i^{U,(t)}$;
6. Calculate $L_{TS}^u((t)) = \sum_{i=1}^{I} (L_{loc}^{(t)} + L_{TS}^{off}(t))$;
7. Update the iterative index $t = t + 1$;
8. Until: $t > T_{max}$ or $|L_{TS}^u((t + 1)) - L_{TS}^u((t))| \leq \delta$;
9. Output: the result to the time allocation, resource allocation, and coefficient matrices optimization

\begin{equation}
\{\mathbf{A}^*, p_i^*, f_i^*, \mathbf{u}_i^{D,*}, \mathbf{u}_i^{U,*}\}\nonumber
\end{equation}

With given time allocation $\mathbf{A}$ and the resource allocation of UEs $\{p_i, f_i\}$, the subproblem of coefficient matrices optimization for STAR-RIS with the TS protocol can be formulated as

\begin{equation}
\max_{\mathbf{u}_i^{D,TS}, \mathbf{u}_i^{U,ES}} \sum_{i=1}^{I} L_{TS}^{off}(t) \nonumber
\end{equation}

\text{s.t.} \quad (8b), (8e) - (8g). \quad (32b)

It can be found that the subproblems of resource allocation of UEs and the coefficient matrices optimization for STAR-RIS with TS protocol have similar structures to the corresponding subproblems (9) and (13) with ES protocol. Therefore, subproblems (31) and (32) can be handled by a similar method to the ES protocol. By iteratively solving subproblems (30)-(32), problem (8) for TS protocol can be solved effectively. Thus, the proposed algorithm for the total computation rate maximization problem with TS protocol can be outlined in Algorithm 6.

D. Convergence, Complexity, and Optimality Analysis

The computational complexity of the proposed Algorithm 4 for ES mainly depends on Algorithm 3. Therefore, we first analyze the computational complexity of Algorithm 3. In Algorithm 3, two subproblems are iteratively solved to obtain $\{f_i, p_i\}$ and $\{\mathbf{u}_i^{D,ES}, \mathbf{u}_i^{U,ES}\}$ with given energy transfer time $\tau_0$. For the UE resource allocation subproblem, it can be solved by the interior point method. Thus, the computational complexity of the optimal solution can be expressed as $O_1 \Delta \leq O \left( L_1 \ln(1/\epsilon) n^2 \right)$, where $n = 2I$ is the number of decision variables and $L_1$ is the number of iterations. For the coefficient matrices optimization subproblem, it can be solved by the SDP method. Denote the number of iterations as $L_2$. The computational complexity can be given by $O_2 = O \left( L_2 \ln(1/\epsilon) (2M)^\Delta \right)$ [13]. Thus, the overall computational complexity of Algorithm 3 can be denoted as $O \left( L_3 (O_1 + O_2) \right)$, where $L_3$ is the number of iterations. Then, in order to obtain the maximum total computation rate of UEs, Algorithm 4 requires to execute a linear search of $\tau_0$ with a small step size $\Delta$ and run Algorithms 3 for $T/\Delta$ times. Thus, the overall complexity of Algorithm 4 also depends on the step size $\Delta$, but it is always polynomial regardless of $\Delta$.

Theorem 3: Algorithm 3 increases the total computation rate of UEs at each iteration and finally converges within a limited number of iterations.

Proof: Denote the objective function of problem (7) for ES with given $\tau_0$ as $L_{ES}^{sum}$. We have

\begin{align}
L_{ES}^{sum} \left( p_i^{(t)}, f_i^{(t)}, \mathbf{u}_i^{D,(t)}, \mathbf{u}_i^{U,(t)} \right) & \leq L_{ES}^{sum} \left( p_i^{(t+1)}, f_i^{(t+1)}, \mathbf{u}_i^{D,(t+1)}, \mathbf{u}_i^{U,(t+1)} \right) \\
& \leq L_{ES}^{sum} \left( p_i^{(t+1)}, f_i^{(t+1)}, \mathbf{u}_i^{D,(t+1)}, \mathbf{u}_i^{U,(t+1)} \right). \quad (33)
\end{align}

The first inequality holds since for fixed coefficient matrices of STAR-RIS $\{\mathbf{u}_i^{D,ES}, \mathbf{u}_i^{U,ES}\}$, the optimal $\{p_i^{(t+1)}, f_i^{(t+1)}\}$ is obtained by solving problem (9) via Algorithm 1; the second inequality follows the fact that the optimal $\{p_i^{(t+1)}, f_i^{(t+1)}\}$ is obtained by solving problem (13) via Algorithm 2 with given $\{p_i^{(t+1)}, f_i^{(t+1)}\}$. Thus, the objective function $L_{ES}^{sum}$ must converge after several iterations. \[ \square \]

Algorithm 4 can be regarded as a repetitive execution of Algorithm 3. Therefore, we only need to guarantee the convergence of Algorithm 3, which has been proved in Theorem 3. Since Algorithm 5 has a similar structure to Algorithm 4, its computational complexity and convergence can refer to Algorithm 4.

Different form Algorithm 4, Algorithm 6 consists of three subproblems. For the time allocation subproblem, it can be solved by linear programming method. Thus, the computational complexity can be given by $O(n_1 \ln n_1)$, where $n_1$ is the number of variables. Thus, given the number of iterations as $L_4$, the overall computational complexity of Algorithm 6 can be expressed as $O \left( L_4 (n_1 \ln n_1 + O_1 + O_2) \right)$, which is in a polynomial time. The convergence of Algorithm 6 is proved in the following Theorem 4.

Theorem 4: Algorithm 6 increases the total computation rate of UEs at each iteration and finally converges within a limited number of iterations.

\begin{equation}
\mathbf{A} = \left[ -\sum_{i=1}^{I} \sum_{r=1}^{K_i} \frac{p_i}{f_i} \frac{K_i}{r^2} \sum_{j \neq r} \frac{p_j |h_j|^2}{\sum_{i \neq r} \frac{p_j |h_j|^2}{\sigma^2} + \sigma^2} \right] \sum_{r=1}^{K_i} \frac{p_i}{f_i} \frac{K_i}{r^2} \left[ 1 + \frac{p_i |h_i|^2}{\sum_{j \neq r} \frac{p_j |h_j|^2}{\sigma^2} + \sigma^2} \right]. \quad (27)
\end{equation}
**Proof:** Denote the objective function of problem (8) for TS as $L_{\text{sum}}^\text{TS}$. We have

$$L_{\text{sum}}^\text{TS} \left( \mathbf{A}^{(t)} p_i^{(t)} f_i^{(t)} u_{k,\text{TS}}^{(t)} u_{k,\text{ES}}^{(t)} \right) \leq L_{\text{sum}}^\text{TS} \left( \mathbf{A}^{(t+1), p_i^{(t+1)} f_i^{(t+1)} u_{k,\text{TS}}^{(t+1)} u_{k,\text{ES}}^{(t+1)} \right) \leq L_{\text{sum}}^\text{TS} \left( \mathbf{A}^{(t+1), p_i^{(t)} f_i^{(t)} u_{k,\text{TS}}^{(t)} u_{k,\text{ES}}^{(t)} \right) \leq L_{\text{sum}}^\text{TS} \left( \mathbf{A}^{(t+1), p_i^{(t+1)} f_i^{(t+1)} u_{k,\text{TS}}^{(t+1)} u_{k,\text{ES}}^{(t+1)} \right) \leq L_{\text{sum}}^\text{TS} \left( \mathbf{A}^{(t+1), p_i^{(t+1)} f_i^{(t+1)} u_{k,\text{TS}}^{(t+1)} u_{k,\text{ES}}^{(t+1)} \right).$$

(34)

The first inequality comes from that $\mathbf{A}^{(t)}$ is solved by linear programming with fixed resource allocation $\left\{ p_i^{(t)}, f_i^{(t)} \right\}$ and coefficient matrices $\left\{ u_{k,\text{TS}}^{(t)}, u_{k,\text{ES}}^{(t)} \right\}$; the second and third inequalities follow the fact that $\left\{ p_i^{(t+1)}, f_i^{(t+1)} \right\}$ and $\left\{ u_{k,\text{TS}}^{(t+1)}, u_{k,\text{ES}}^{(t+1)} \right\}$ are optimal solutions to subproblem of UEs’ resource allocation and the subproblem of coefficient matrices optimization for STAR-RIS, respectively. Considering that the total computation rate is upper-bounded, the objective function $L_{\text{sum}}^\text{TS}$ converges after several iterations. ■

The proposed algorithms in our manuscript can achieve the suboptimal solution in polynomial time. Take Algorithm 4 as an example, where the linear search method is exploited to obtain $\tau_0^*$. It is worth noting that the optimality gap can be ignored when the step size approaches zero. Then, with given $\tau_0^*$, Algorithm 3 is executed to obtain the solution to resource allocation and configuration design of STAR-RIS in an alternative manner. Algorithm 3 is a typical block coordinated descent (BCD) algorithm, and it can achieve the local optimum with a fast convergence speed, which has been adopted to tackle various non-convex optimization problems in wireless communication systems. Therefore, based on above analysis, the suboptimal solution to problem (7) with TS protocol can be obtained by our proposed Algorithm 4. Since the algorithms for MS and TS protocols have similar structures to Algorithm 4, they can also achieve the suboptimal solution in polynomial time.

V. SIMULATION RESULTS

In this section, simulation results are provided to evaluate the performances of the proposed algorithms for the total computation rate maximization problems in the STAR-RIS-enhanced wireless-powered MEC system. To ensure a fair comparison, one reflecting-only RIS and one transmitting-only RIS are employed at the same location as the STAR-RIS to play as the baseline scheme (referred to as the conventional RIS) and achieve the full-space coverage [13], where both the reflecting-only RIS and the transmitting-only RIS have $M/2$ elements. In addition, all UEs have the same configurations with the non-linear energy harvesting model parameters given by $a_i = 1500, b_i = 0.0022$, and $\psi_i = 80$ mW [28].

In the simulations, the AP and the STAR-RIS are located at $(0, 0, 0)$ meters and $(0, 10, 0)$ meters, respectively [43]. The UEs are randomly distributed on a circle centered at the STAR-RIS with a radius of $r = 3$ m.

The communication links from UEs to STAR-RIS and that from STAR-RIS to the AP are modeled as Rician fading channels, which can be expressed as

$$h = \sqrt{\rho d^{-\alpha}} \left( \frac{\gamma}{1 + \gamma} h_{\text{LoS}} + \frac{1}{1 + \gamma} h_{\text{NLoS}} \right),$$

(35)

where $\rho$ is the path loss at the reference $D = 1$m. $d$ denotes the distance between the wireless transmitter and the corresponding receiver. $\alpha$ represents the path loss factor of communication link and $\gamma$ indicates the Rician factor. $h_{\text{LoS}}$ and $h_{\text{NLoS}}$ are the LoS component and NLoS component of the corresponding channel, respectively [43]. The other simulation parameters are summarized in Table I.

Fig. 3 and Fig. 4 demonstrate the convergence behaviors of the proposed algorithms for ES, MS, and TS protocols, where $T = 1$s. For ES and MS protocols, the energy transfer time is given by $\tau_0 = 0.2s$. It can be observed that the total computation rates of three protocols are monotonically increased at each iteration, and the algorithms finally converge after several iterations, which verifies the convergence analysis in Theorems 3 and 4. Besides, as expected, with the increase of $M$, the computation rates of three protocols are increased since more DoFs for transmission and reflection design can be exploited. Meanwhile, under different numbers of STAR-RIS elements, the proposed algorithm can still converge with a fast rate.

| TABLE I |
| SIMULATION PARAMETERS [27], [43] |
|---|---|
| Parameters | Default Values |
|---|---|
| Total bandwidth, $B$ | 20 MHz |
| Noise power, $\sigma^2$ | -90 dBm |
| Rician factor, $\gamma$ | 3 dB |
| UEs’ maximum transmit power, $P_{\text{max}}$ | 0.1 W |
| UEs’ maximum CPU frequency, $f_{\text{max}}$ | 8 GHz |
| Effective capacitance coefficient, $\kappa$ | $10^{-29}$ |
| The tolerant threshold, $\epsilon, \delta$ | $10^{-8}$ |
| Path loss factor, $\alpha$ | 2.2 |

Fig. 3. The total computation rate of UEs versus the iteration index for the ES and MS protocols.

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The total computation rate of UEs first increases as \( \tau_0 \) grows, and then starts to decrease after \( \tau_0 \) is larger than a threshold. The reasons behind this phenomenon can be explained as follows. When \( \tau_0 \) is smaller, UEs can only harvest fewer energy for task offloading and local computing. Accordingly, the total computation rate of UEs is lower. Then, with the increase of \( \tau_0 \), more energy can be harvested by UEs and thus more task bits can be offloaded to the AP or computed locally at UEs, which leads to the increase of the total computation rate. However, when \( \tau_0 \) is further increased, the rest time of the mission period used for local computing and task offloading is continuously decreased. Hence, the total computation rate of UEs is also decreased. In addition, we also observe that the optimal energy transfer time \( \tau_0^* \) that results in the maximum total computation rate of UEs increases with the growth of the mission period. This is because with a larger mission period, UEs have enough time for local computing and task offloading.

Thus, \( \tau_0^* \) can be increased such that UEs can harvest more energy to increase the transmit power for task offloading and the CPU frequency for local computing, thereby achieving a larger computation rate.

In Fig. 6, the total computation rate of UEs versus the transmit power of the AP is demonstrated, where \( T = 1 \) s and \( M = 10 \). As expected, the total computation rate of UEs increases as the AP’s transmit power increases for all schemes. This is because when the AP transfers energy to UEs with a larger power, the UEs can harvest more energy and thus more computation tasks can be executed via task offloading and local computing. Besides, it can be observed that the conventional RIS always has the worst performance in terms of total computation rate compared with the three protocols of STAR-RIS. The reason is that compared to the conventional RIS which can only control the phase shift, the STAR-RIS has more adjustable parameters and these parameters provide extra DoFs to further enhance the offloading channel conditions of UEs. By fully exploiting these DoFs, the STAR-RIS can always achieve a higher computation rate than the conventional RIS. Moreover, regarding the three protocols for STAR-RIS, the TS protocol can achieve the best performance in comparison with the ES and MS protocols. This is because the opposite-side leakage of ES/MS protocol leads to the waste of UEs’ transmit power, and hence decreases the total computation rate. As a contrast, for the TS protocol, although the offloading time is reduced due to the STAR-RIS’s time allocation for reflection and transmission modes, the UEs are always served by all elements and there is no energy leaked to the opposite side of the STAR-RIS during the task offloading. Meanwhile, if the TS protocol is employed at the STAR-RIS, the interference among UEs can be greatly reduced compared to the ES and MS protocols since the inter-user interference at the AP only comes from the UEs in the transmission/reflection space, i.e., only half-space interference exists. On the contrary, if the ES or MS protocol is employed, the inter-user interference comes from all UEs located both in the transmission space and the reflection space.
i.e., there exists full-space interference. Thus, the interference is more severe at the AP and the total computation rate of UEs is decreased. In addition, it can also be observed that the ES protocol outperforms the MS protocol since the MS protocol is a special case of ES protocol from the mathematical perspective, as we state in problem (7).

Fig. 7 shows the impact of the mission period $T$ on the total computation rate of UEs. It is observed that the total computation rate increases with the growth of the mission period. This is because when the mission period increases, the energy transfer time and the energy harvested by UEs also increase, which provides more energy supplies for UEs to execute more task bits. Besides, with a larger mission period, the task offloading and local computing can be executed with longer time, which further increases the total computation rate of UEs. It is also observed that the STAR-RIS outperforms the conventional RIS and the TS has the best performance, which coincides with the results shown in Fig. 6.

Fig. 8 presents the total computation rate of UEs versus the number of RIS’s elements. It can be found that the total computation rate of UEs increases with the number of RIS’s elements. Moreover, we also observe that the performance gap between the STAR-RIS and conventional RIS becomes larger as the number of RIS’s elements increases. The reason is that when the number of RIS elements increases, the additional elements can provide more opportunities for designing more efficient configuration strategy of STAR-RIS, and thus a higher performance gain can be achieved.

In Fig. 9, we study the impacts of the CPU cycles required for computing 1-bit of task-input data ($C_i$) on the total computation rate of UEs. It is observed that the total computation rate decreases with the increase of $C_i$. Apparently, when $C_i$ increases, the energy consumed for executing 1-bit task data via local computing will be increased. Thus, with the limited energy harvested from the AP, the amount of task bits computed locally by UEs decreases. Accordingly, the total computation rate of UEs is also decreased.

In Fig. 10, the total computation rate of UEs is shown against the number of UEs. To ensure a fair comparison, there are the same number of UEs in the transmission space and reflection space. From Fig. 10, it can be found that the
total computation rate of UEs decreases with the increase of the number of UEs. The reason is that when the UEs perform task offloading, the NOMA protocol is applied, which allows all UEs to access the AP and offload task bits at the same time and frequency. Thus, the inter-user interference becomes more severe with larger number of UEs, which leads to the degradation of the total computation rate. We can also see that the proposed algorithms for STAR-RIS can always achieve larger computation rate than the conventional RIS under different number of UEs, which further verifies the superiority of STAR-RIS. Meanwhile, the performance gap among the ES, MS, and TS highlights the importance of employing proper operating protocol in the wireless-powered MEC systems.

VI. CONCLUSION

In this paper, the STAR-RIS-enhanced wireless-powered MEC system has been investigated, where the STAR-RIS was deployed to assist UEs’ task offloading and AP’s energy transfer. The total computation rate of UEs was maximized by jointly optimizing the energy transfer time, transmit power and CPU frequencies of UEs, and the design configuration of STAR-RIS. Three operating protocols of STAR-RIS were considered during the task offloading. To solve the formulated non-convex problems, based on the penalty method, the SCA technique and the linear search method, an iterative algorithm was proposed to solve the ES problem. Then, the proposed algorithm for ES protocol was extended to solve the MS and TS problems. Simulation results revealed that the STAR-RIS outperformed the traditional reflecting/transmitting-only RIS. More importantly, the TS protocol can achieve the largest computation rate among the three operating protocols of STAR-RIS.

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