Adsorption of Fatty Acid Molecules on Amine-Functionalized Silica Nanoparticles: Surface Organization and Foam Stability

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ABSTRACT: The crucial roles of the ionization state and counterion presence on the phase behavior of fatty acid in aqueous solutions are well-established. However, the effects of counterions on the adsorption and morphological state of fatty acid on nanoparticle surfaces are largely unknown. This knowledge gap exists due to the high complexity of the interactions between nanoparticles, counterions, and fatty acid molecules in aqueous solution. In this study, we use adsorption isotherms, small angle neutron scattering, and all-atom molecular dynamic simulations to investigate the effect of addition of ethanolamine as a counterion on the adsorption and self-assembly of decanoic acid onto aminopropyl-modified silica nanoparticles. We show that the morphology of the fatty acid assemblies on silica nanoparticles changes from discrete surface patches to a continuous bilayer by increasing concentration of the counterion. This morphological behavior of fatty acid on the oppositely charged nanoparticle surface alters the interfacial activity of the fatty acid–nanoparticle complex and thus governs the stability of the foam formed by the mixture. Our study provides new insights into the structure–property relationship of fatty acid–nanoparticle complexes and outlines a framework to program the stability of foams formed by mixtures of nanoparticles and amphiphiles.

1. INTRODUCTION

The aggregative adsorption of amphiphilic molecules on colloids governs the optical properties, interfacial activity, and stability of the particles in the dispersion.1−9 The self-assembled state of amphiphilic molecules on colloidal particles is dependent on the interaction between: (1) particle surface and unadsorbed amphiphilic molecules, (2) amphiphilic molecules adsorbed on the surface and unadsorbed molecules in bulk solution, and (3) among the molecules adsorbed on the surface.7−9 These interactions determine the morphology of surface-adsorbed aggregates of amphiphilic molecules and govern the interfacial activity of the colloidal particles with adsorbed amphiphiles. The adsorption mechanism and morphology of the surface aggregates formed by synthetic amphiphiles, such as non-ionic surfactants, onto hydrophilic nanoparticles are well-known and characterized.10−12 However, the equilibrium morphology of natural amphiphiles, such as fatty acids, adsorbed onto nanoparticles in the presence of organic counterions and their impact on the interfacial activity of nanoparticles are poorly understood. This lack in understanding is due to the complexity of the phase behavior of fatty acid molecules on the nanoparticles, which is highly dependent on the concentration of counterions in the dispersion medium.13,14

Fatty acids are a class of naturally occurring amphiphiles consisting of an aliphatic hydrocarbon chain and carboxylic acid polar head group.15 The carboxylic acid head group can exist in either the protonated (−COOH) or deprotonated (−COO−) state, which is primarily governed by the presence of counterion molecules in solution.16 The concentration of the counterion in the solution also governs the morphology of the self-assembled state of the fatty acid molecules and their Kraft temperature. Previously, it has been shown that increasing the fatty acid-to-counterion molar ratio in aqueous solution drives morphological transitions in the self-assembled state of the fatty acids from disc-like micelles, to multilamellar tubules, to discrete spherical micelles.17,18 Despite the rich phase behavior of the fatty acid molecules in bulk, the effects of the ionization state of fatty acids on their adsorption onto hydrophilic nanoparticles remain unknown. The self-assembled state and phase behavior of fatty acid in aqueous solution...
containing nanoparticles are impacted by the chemical design of the fatty acid molecules, size of the nanoparticles, and environmental parameters such as temperature, salinity, and the presence of counterions.19–21 Understanding the interactions governing the self-assembly and phase behavior of fatty acids adsorbed at nanoparticles is critical to the development of multifunctional materials with tunable interfacial and bulk properties, such as foam stability and viscoelasticity.22 In this study, we systematically probe the effect of increasing counterion concentration on the adsorption and self-assembled state of fatty acid molecules on the surface of hydrophilic nanoparticles, and investigate its corresponding impact on the interfacial activity of the fatty acid–nanoparticle complex.

We use adsorption isotherm, small angle neutron scattering (SANS), and all-atom molecular dynamic (MD) simulations to understand the effect of an increasing concentration of counterions on the adsorbed amount, and the morphology of the fatty acid molecules formed at amine functionalized hydrophilic nanoparticles. We use decanoic acid (C10H20COOH) and ethanolamine (HOCH2CH2NH2) as model fatty acid molecules and counterions, respectively, and propyl amine (C9H19NH2)-functionalized spherical silica (mSiO2) as model hydrophilic nanoparticles. We find that the counterion-to-fatty acid molar ratio not only determines the amount of fatty acid adsorbed on the silica nanoparticles but also governs the morphology of the fatty acid assemblies formed at the mSiO2 surface. Furthermore, we demonstrate that the morphological change of fatty acid at mSiO2 impacts the interfacial activity of the composite structure, thus altering the stability of foam formed by the dispersion. This study outlines the relationship of the counterion-tuned structure of fatty acid assemblies on silica nanoparticles to the interfacial activity of the composite structure, and provides insights into the principle of designing nanomaterials with tunable foaming properties.

2. RESULTS AND DISCUSSION

2.1. Nanoparticle Synthesis and Characterization.

2.1.1. Amine Functionalization of Silica Nanoparticles.

The propylamine-functionalized silica nanoparticles were synthesized by controlled surface modification of commercially available Ludox-TMA colloidal silica (Sigma-Aldrich). The silica nanoparticle dispersion was dialyzed for 7 days using ultrapure water with a resistivity of 18.2 MΩ-cm, changing water every day to remove any undesired foreign molecules in the dispersion. In a typical synthesis, 22.2 g of 27 wt % Ludox-TMA dispersion was mixed with 12 mL of acetic acid and 3.8 mL of deionized water (Figure 1a and Figure S1). The mixture was transferred into a round-bottom flask, fitted with a reflux condenser, and heated to 80 °C. After 30 min of equilibration, 0.7 mL of (3-aminopropyl)triethoxysilane (APTES) was added to the flask containing the mixture with constant stirring. The mixture was reacted for 16 h at 80 °C under reflux. The dispersion containing modified silica nanoparticles was removed from the flask and dialyzed for 24 h using deionized water at pH 4. The larger aggregates from the dialyzed mSiO2 were removed by filtering it through a syringe filter with a pore size of 220 nm. The pH of the filtered nanoparticle solution was adjusted to 4, and the mSiO2 dispersion was stored at 4 °C.

2.1.2. Characterization of mSiO2.

The mSiO2 nanoparticles were characterized for their size and surface charge by small angle X-ray scattering (SAXS), a scanning electron microscope (SEM), and zeta potential–pH titration. The bulk size characterization of mSiO2 was performed using SAXS (Xenocs Xeuss 2.0). The SAXS profiles for 0.1% by weight of mSiO2 at pH 7 is shown in Figure 1b where I(q) is the scattering intensity, and q is the scattering momentum transfer related to the X-ray wavelength (λ) and scattering angle (θ) as $q = \left( \frac{4\pi}{\lambda} \right) \sin \left( \frac{\theta}{2} \right)$. The experimentally measured scattering profile is fitted using a spherical form factor model with log-normal particle size distribution (Figure 1b). The form factor model is effective in representing the scattering at q > 0.2 nm⁻¹ but fails in the region q < 0.2 nm⁻¹. This disagreement between the experimental data and form factor model is caused by weak aggregation of the nanoparticles at pH 7 (zeta potential < +15 mV, Figure 1c), which results in an increase in scattering intensity at q < 0.2 nm⁻¹. Despite the presence of the structure factor, the form factor provides the accurate nanoparticle diameter of 30 nm, with a polydispersity index of 0.1, which agrees with SEM imaging (Figure 1b, inset). The surface charge on mSiO2 is quantified using zeta potential measurement (Litesizer 500, Anton Paar GmbH) as a function of pH (Figure 1c). The experimental results show that the zeta potential of mSiO2 changes from +42.7 to −31.1 mV as pH is increased from 2 to 11, and the isoelectric point of mSiO2...
nanoparticles is pH \( \sim 8.5 \). The isoelectric point of the native silica nanoparticles is pH \( \sim 2 \), but it changes to pH \( \sim 8.5 \) upon surface modification with propylamine surface groups (Figure S1). The change in the isoelectric point of silica nanoparticles upon surface chemical modification is attributed to the protonation of the aminopropyl functional group at pH < 8. The positive charge on the surface of \( m\text{SiO}_2 \) at pH < 8 is key in directing the adsorption and corresponding self-assembled state of the fatty acid molecules on the surface of \( m\text{SiO}_2 \) nanoparticles.

2.2. Adsorption of Fatty Acid on \( m\text{SiO}_2 \).

In this study, we use decanoic acid as model fatty acid and control its protonation state using ethanolamine as a counterion. We define the counterion-to-fatty acid molar ratio (\( R \)) as the ratio of the total number of ethanolamine to the fatty acid molecules in the solution. The value of \( R \) is equivalent to the fraction of the fatty acid molecules in the deprotonated state, i.e.,

\[
R = \frac{n_{\text{COO}^-}}{n_{\text{total}}} \tag{1}
\]

where \( n_{\text{COO}^-} \) is the number of deprotonated fatty acid molecules, and \( n_{\text{total}} \) is the total number of fatty acid molecules in the solution. To understand the effect of the ionization state of fatty acid on its interaction with \( m\text{SiO}_2 \), we experimentally measure the adsorption isotherms of the decanoic acid onto \( m\text{SiO}_2 \) nanoparticles with \( R \) increasing from 0.05 to 1.0. The adsorption isotherms were measured at pH 6, where the net charge on \( m\text{SiO}_2 \) is positive and an electrostatic attraction exists between the deprotonated carboxylate group of the fatty acid and protonated propyl ammonium group on the surface of \( m\text{SiO}_2 \) nanoparticles.

The adsorption isotherms were measured using a well-established solvent depletion method. In a typical adsorption experiment, increasing amounts of fatty acid at fixed \( R \) were added to 1 wt % \( m\text{SiO}_2 \) aqueous dispersion. The pH was adjusted to 6 by adding small amounts of 5 N aqueous HCl or NaOH solution. The mixture was equilibrated at 20 °C for 24 h, and then \( m\text{SiO}_2 \) with adsorbed fatty acid molecules was removed by centrifuging the dispersions at 18,000 RCF for 2 h. Electrostatic attraction between the oppositely charged fatty acid molecules and silica surfaces further drives fatty acid-mediated aggregation of \( m\text{SiO}_2 \) nanoparticles, thus destabilizing the dispersion. The aspect of aggregation of \( m\text{SiO}_2 \) nanoparticles into fractal superstructures, while interesting, is beyond the scope of this study focused on understanding the self-assembly of fatty acid molecules on nanoparticles.

Based on visual inspection of the sample and known adsorption mechanism of amphiphiles, fatty acid molecules in their mixture with counterions and \( m\text{SiO}_2 \) are present in three distinct forms, namely, (a) undissolved fatty acid gel (\( c_u \) protonated form, \(-\text{COOH}\)), (b) unadsorbed fatty acid in bulk solution (\( c_d \) deprotonated form, \(-\text{COO}^-\)), and (c) adsorbed fatty acid onto \( m\text{SiO}_2 \) (\( c_{\text{ads}} \) deprotonated form, \(-\text{COO}^-\)) as shown in Figure 2a. The fractions of total fatty acid concentration (\( c_t \)) existing in these three forms were determined by systematically separating the mixture using centrifugation. The mass density of the native protonated fatty acid is \( \sim 0.893 \) g/cm\(^3\); therefore, the concentration of fatty acid in the undissolved gel form (\( c_u \)) was determined by physically collecting the pellets floating on the liquid–air interface in the vial after centrifugation. The pellets were dried overnight at room temperature to ensure complete evaporation of water. The concentration of undissolved fatty acid decreases with increasing \( R \), as shown in Figure S2. The concentration of fatty acid dissolved in aqueous solution but unadsorbed onto \( m\text{SiO}_2 \) was determined by first carefully removing the aqueous supernatant from the centrifuged sample and then measuring the concentration of the fatty acid in the supernatant using surface tension. The surface tension of the supernatant was measured using an optical tensiometer (Attension Theta, Biolin Scientific) where the shape of the pendant droplet is analyzed using Young–Laplace equation.

The relationship between surface tension and concentration of the fatty acid in the supernatant was determined for different solutions with known concentrations, yielding a calibration curve, as shown in Figure S3. When the unknown concentration of deprotonated fatty acid in the supernatant was higher than critical micellization concentration (CMC) of the molecules, the unknown concentration was determined by systematic dilutions until the measured surface tension is below its characteristic value at CMC. The net unknown concentration of the supernatant was calculated by multiplying the concentration estimated for the diluted sample (from surface tension calibration curve) and the dilution factor. It should be noted that fatty acid molecules only in the deprotonated state (\(-\text{COO}^-\)) are surface-active and reduce the surface tension, as shown in Figures S3 and S4. Therefore, the surface tension measurements enable selective determination of concentration of fatty acid molecules in the dissolved (deprotonated) state.

The amount of fatty acid molecules adsorbed onto \( m\text{SiO}_2 \) nanoparticles (\( \Gamma \)) is obtained from the equation

\[
\Gamma = c_{\text{ads}}V/m \tag{2}
\]

where \( V \) is the volume of the aqueous solution, \( m \) is the mass of \( m\text{SiO}_2 \) in bulk solution, \( c_{\text{ads}} = c_t - (c_u + c_d) \) is the concentration of fatty acid molecules adsorbed onto \( m\text{SiO}_2 \), \( c_t \) is the total concentration of fatty acid, \( c_u \) is the concentration of dissolved but unadsorbed fatty acid in the solution, and \( c_d \) is the concentration of undissolved fatty acid molecules (Figure 2a). It should be noted that for \( R = 1 \), the value of \( c_u = 0 \), i.e.,
all fatty acid exists in dissolved states, i.e., undissolved and adsorbed states on nanoparticles (deprotonated form, −COO⁻) and for R = 0, c_p = c_f, i.e., the fatty acid molecules exist only as an undissolved gel state (protonated form, −COOH). The adsorption isotherms of fatty acid molecules bound to mSiO₂ nanoparticles at five R values are shown in Figure 2b. At all tested counterion concentrations, the amount of fatty acid adsorbed on mSiO₂ shows an initial increase followed by a plateau, which is a characteristic of the molecular adsorption on a surface with a fixed number of binding sites. These experimentally measured adsorption isotherms can be represented by a Langmuir adsorption model given as

\[ \Gamma = \frac{\Gamma_{\text{max}} K_{\text{ads}} c_f}{1 + K_{\text{ads}} c_f} \]  

(1)

Here, \( \Gamma \) is the amount of fatty acid adsorbed onto mSiO₂, \( \Gamma_{\text{max}} \) is the maximum surface excess of fatty acid, \( c_f \) is the equilibrium concentration of dissolved but undissolved fatty acid in bulk, \( K_{\text{ads}} \) is the equilibrium adsorption constant, which is proportional to the binding affinity of the fatty acid molecules to mSiO₂ nanoparticles. The Langmuir model is the simplest two-parameter model that allows representing the maximum amount of fatty acid adsorbed and its binding affinity for mSiO₂ in terms of \( \Gamma_{\text{max}} \) and \( K_{\text{ads}} \).

The experimental adsorption isotherm data are fitted using the Langmuir model given in eq 1 (Figure 2b) keeping \( \Gamma_{\text{max}} \) and \( K_{\text{ads}} \) as free fit parameters. The values of \( \Gamma_{\text{max}} \) and \( K_{\text{ads}} \) as obtained by the least square fitting of experimental data with increasing \( R \) are shown in Figure 2c,d. We find that \( \Gamma_{\text{max}} \) increases (nearly) linearly with increasing \( R \). The values of \( \Gamma_{\text{max}} \) increased from 1.0 to 16.0 nmol/m² (Figure 2c) as \( R \) increased from 0.05 to 1.0, i.e., the number of fatty acid molecules adsorbed onto mSiO₂ increases with increasing \( R \). The observed linear increase in the maximum surface excess of fatty acid molecules can be attributed to the linear increase in the concentration of deprotonated (negatively charged carboxylate) fatty acid molecules with increasing \( R \).

We find that \( K_{\text{ads}} \) shows only a slight increase from 0.4 to 1.4 mM⁻¹ with \( R \) increasing from 0.05 to 1.0. This slight increase in \( K_{\text{ads}} \) with \( R \) is an indicative of the small increase in adsorption free energy of the fatty acid molecules at the mSiO₂ surface. It should be noted that because pH of the aqueous solution was kept fixed (at pH 6), the surface charge of mSiO₂ can be approximated as constant for all \( R \). Assuming that the charging of the silica and fatty acid molecules involves monovalent ions only and that the surface change density of mSiO₂ at pH 6 is low, the free energy of adsorption can be calculated from \( K_{\text{ads}} \) as \( \Delta G_{\text{ads}} = -N_A k_B T \ln(55.5 \times K_{\text{ads}}) \) where \( N_A \) is the Avogadro number, \( k_B \) is the Boltzmann constant, and \( T \) is the temperature. We find that the magnitude of \( \Delta G_{\text{ads}} \) increases from −24.2 to −27.4 kJ/mol upon increasing \( R \) from 0.05 to 1.0. Two key conclusions drawn from these values are: first, the value of \( \Delta G_{\text{ads}} \) is lower than the adsorption free energy of cationic surfactants on the silica surface. This lowering of adsorption free energy in our case can be attributed to the smaller surface charge density on the synthesized mSiO₂ nanoparticles. Second, only a small increase in \( \Delta G_{\text{ads}} \) highlights that the chemical nature of the functional group binding to mSiO₂ at low and high \( R \) values is similar, which is the carboxylate group of the decanoic acid. The adsorption isotherms show that the amount of fatty acid bound onto mSiO₂ increases but do not provide any insights into the self-assembled state and morphology of the surface-adsorbed molecules. To uncover the self-assembled state of the fatty acid on mSiO₂ nanoparticles, we perform small angle neutron scattering analysis for dispersions of mSiO₂ with adsorbed fatty acid, as discussed in the next section.

2.3. Morphology of Fatty Acid Adsorbed onto mSiO₂. 2.3.1. Small Angle Neutron Scattering Experiments. An increase in the counterion-to-fatty acid molar ratio leads to an increase in the amount of fatty acid molecules adsorbed on mSiO₂ nanoparticles. This increase in surface adsorption of fatty acid molecules drives a morphological change in the fatty acid assemblies formed on the surface of mSiO₂ nanoparticles. Here, we characterize the morphology of the fatty acid molecules on mSiO₂ using SANS. The experiments were carried out at silica contrast-matched condition where 62.5 wt % deuterium oxide (D₂O) and 37.5 wt % H₂O were used as the solvent. Therefore, the neutron scattering originated solely from the fatty acid molecules and their assemblies in the solution. The SANS experiments were performed at ORNL HFIR facility using the GP-SANS instrument with pinhole collimation at a neutron wavelength of 6 Å. Further details about the SANS experiments can be found in previous publications.

The SANS experiments were performed at constant total concentrations of fatty acid and mSiO₂, with increasing counterion-to-fatty acid molar ratio from \( R = 0.05 \) to 1.0. The maximum concentration of fatty acid molecules adsorbed onto silica at \( R = 1.0 \) is given by

\[ C_{\text{max}} = \frac{\Gamma_{\text{max}} A_{\text{mSiO}_2} W_{\text{mSiO}_2}}{V_{\text{total}}} \times 10^{-3} \]  

(2)

where \( C_{\text{max}} \) is the total concentration of fatty acid at \( \Gamma_{\text{max}} \), \( A_{\text{mSiO}_2} \) and \( W_{\text{mSiO}_2} \) are the specific surface area and weight of mSiO₂ nanoparticles in the solution, respectively, and \( V_{\text{total}} \) is the total volume of the sample. Here, the fatty acid concentration was 0.03 M, which was equivalent to the 0.5 \( C_{\text{max}} \) at \( R = 1.0 \) (Figure 2b). Therefore, for SANS at \( R < 1.0 \) the fatty acid existed in three states as discussed in the previous section (Figure 2a). The undissolved fatty acid floats on the surface of the solution; therefore, the incoming neutron beam selectively probes the protonated fatty acid in the aqueous solution (both adsorbed and undissolved). The SANS profiles for mSiO₂ with adsorbed fatty acid under silica contrast-matched conditions with increasing \( R \) at pH 6 and 20 °C are shown in Figure 3a. The mSiO₂ nanoparticles in the presence of fatty acid exist as aggregates and tend to phase separate. During our SANS measurements, these aggregates settle and only a small unknown fraction of the particles with adsorbed fatty acid remain in the neutron beam. Because of the lack of information of the exact amount of the silica−fatty acid composite in the neutron beam, the scattering intensity is represented in arbitrary units. The curves show an increase in the low-\( q \) (\(< 0.15 \text{ nm}^{-1}\)) scattering with I(\( q \) \( \propto \) \( q^{-2} \)). This proportional increase in the scattering intensity is likely a combination of the scattering due to the fatty acid-mediated aggregation of mSiO₂ nanoparticles, and the presence of fatty acid gel phase clusters in the solution. The SANS profiles also show enhancement of the primary form factor oscillation at \( q \sim 0.15 \text{ nm}^{-1} \) with increasing \( R \). Additionally, the primary minima show a slight shift to higher \( q \) values upon increasing \( R \) (Figure 3b), indicating a decrease in the size of fatty acid assemblies on mSiO₂ nanoparticles. Detailed characteristics of
self-assemblies formed by molecules on nanoparticles can be obtained by fitting the experimental SANS data to theoretical form factor models. In our case, such model dependent analysis is not feasible because of too many unknown and unconstrained fit parameters. Therefore, we first perform model independent analysis of the SANS data using Porod’s law and determine the change in the surface-to-volume ratio of the fatty acid assemblies with increasing $R$. According to Porod’s law, the scattering intensity at large $q$ ($\to \infty$) is represented as $I(q) = \frac{2\pi(D_1)^2}{\bar{V}}$ where $D_1$ is the scattering length density contrast between the scattering object and surrounding medium, and $\bar{V}$ is the surface area-to-volume ratio of the scattering object. Analyses of our SANS data (Figure S5) show approximately 10 times increase in the $\bar{V}$ upon increasing $R$ from 0.05 to 1.0. This increase in surface-to-volume ratio indicates a significant decrease in the size of self-assembled structures formed by fatty acid, highlighting a phase transition of fatty acid from the bulk gel phase to surface-adsorbed layer upon increasing counterion concentration. Note that since scattering intensity is in arbitrary units, the observed increase in the values of $\bar{V}$ with increasing $R$ only represents qualitative changes. A complete model-dependent SANS data analysis is limited due to the fatty acid-induced aggregation of $mSiO_2$ nanoparticles and corresponding emergence of the structure factor in the scattering profile, which requires additional parameters. Therefore, instead of direct fitting the experimental data, we systematically simulate the SANS profiles, which provide a qualitative information on the morphology of the assemblies formed by fatty acid molecules on $mSiO_2$ nanoparticles.

Previous studies have shown that amphiphilic molecules can adsorb onto nanoparticles in two morphological states, namely, continuous layers or discrete patches.

To investigate which of the two morphologies is formed by fatty acid molecules on $mSiO_2$, we test the applicability of the spherical shell and raspberry-like form factor models in representing the experimental SANS profiles. The spherical shell model represents the formation of a continuous layer of fatty acid on $mSiO_2$ nanoparticles. Here, we simulate the SANS profiles using a shell model with a fixed core radius of 15 nm with a 0.1 polydispersity index (Figure 1b) and increasing the shell thickness from 0.6 to 3.0 nm (Figure 3c). These thickness values are used because of the characteristic length of the decanoic acid molecule, which is 1.2 nm; therefore, 1.2 nm and 2.4 nm correspond to continuous homogeneous monolayer and bilayer structures, respectively. We find that the primary oscillation at $q \sim 0.25$ nm$^{-1}$, a characteristic of the shell structure, is present in all simulated cases, which is in qualitative disagreement with the experimental SANS profiles (Figure 3a,b) for $R < 0.5$. The experiments show the presence of a smeared oscillation at $R < 0.5$. This qualitative mismatch between the experimental and simulated SANS profiles suggests that the self-assembled state of the fatty acid on $mSiO_2$ is more complex than a continuous shell of fatty acid molecules formed on nanoparticles.

The second possible morphological state of fatty acid on $mSiO_2$ nanoparticles is discrete patches. Here, we test the presence of such configuration of fatty acid on the nanoparticles by simulating the scattering profile using a raspberry-like form factor. The model represents the form factor of a large sphere with small spheres randomly adsorbed on its surface. The total scattering intensity of such a raspberry-like structure with a core particle contrast-matched with the continuous medium is given as

$$I_{RB}(q) = \frac{N\phi_i V_s^3 \Delta\rho^2 \Psi_s^2}{16V_i} \left[ 1 + (N - 1) \left( \frac{\sin(q(r_i + r_s))}{q(r_i + r_s)} \right)^2 \right]$$

$$\Psi_s = \frac{3|\sin(qr_i) - qr_i\cos(qr_i)|}{(qr_i)^2}$$

where $N$ is the number of small spheres of radius $r_s$, volume $V_s$ and scattering contrast $\Delta\rho$ adsorbed onto the core particle, $\phi_i$ is the volume fraction of the core particle of radius $r_i$, volume $V_i$, and $q$ is the scattering vector (see the Supporting Information for detailed derivation). The raspberry-like form factor model accounts for all the self-correlation and cross-correlation for small spheres randomly adsorbed onto a larger sphere. The simulated SANS profiles for a contrast-matched sphere with an increasing number of surface-adsorbed smaller spheres are shown in Figure 3d. The profiles are simulated for core particle radius $r_i = 15$ nm, $r_s = 4$ nm with increasing $N$ from 12 to 200. The simulated curves using raspberry-like form factor show an oscillation in the range $0.15 < q < 0.3$ nm$^{-1}$. This oscillation is the signature of the characteristic correlation

Figure 3. (a) SANS profiles for fatty acid molecules adsorbed on $mSiO_2$ nanoparticles in H$_2$O/D$_2$O mixture matching the scattering length density of silica. The profiles were measured at increasing $R$ from 0.05 to 1.0. The curves are shifted by a constant factor of 10 for better visualization. (b) Zoomed-in plot of the scattering intensity from $q = 0.07$ to 1 nm$^{-1}$. The primary minima of SANS profile shifts to higher $q$ values upon increasing $R$, indicating a decrease in the characteristic size of the self-assemblies formed by fatty acid molecules on $mSiO_2$ upon increasing counterion concentration. (c) Simulated SANS profiles using spherical shell and raspberry-like form factor models, respectively. The spherical shell form factor model provides poor representation of the experimental data (shown in (a)) both qualitatively and quantitatively. The primary oscillation of raspberry-like form factor model qualitatively represents the experimental SANS data and captures the change in the morphology of adsorbed fatty acid. The inserts in (c) and (d) are the respective conceptual schematics of the used form factor models.
distance between the surface adsorbed small spheres. The oscillation gets pronounced upon increasing $N$ because of the increasing correlation in spatial distribution of the surface-adsorbed particles (fatty acid in our case), which is the characteristic diameter of the core particle (Figure 3d). The observed behavior of smearing of the primary oscillation at low $N$ is characteristic of the nature of the surface adsorbed structures. At large $N$, the surface assembly of fatty acid resembles the continuous layer, and the spherical shell and raspberry-like form factor models yield similar results (Figure 3b,c). We acknowledge that the raspberry-like form factor is strictly applicable only in the case of spherical particles adsorbed onto a larger sphere, the model qualitatively captures the effect of the discrete nature of the surface-adsorbed assemblies on the scattering profile, especially at low surface loadings. In our experiments of fatty acid adsorbed on $m$SiO$_2$, we observe similar smearing of the primary form factor oscillation at $R < 0.25$, highlighting the discrete nature of the fatty acid assemblies formed on $m$SiO$_2$ nanoparticles. Upon increasing the counterion concentration to $R$ above 0.50, the oscillation becomes pronounced, which agrees with the continuous layer of fatty acid molecules on the nanoparticles. At $0.25 < R < 0.50$, the SANS profile shows a behavior intermediate between discrete patches and continuous layer, which is critical in programming the interfacial binding of the fatty acid-nanoparticle complex (discussed in section 2.5). In summary, the SANS shows that the morphology of the fatty acid adsorbed on the $m$SiO$_2$ nanoparticles changes from discrete patches to the continuous layer upon increasing $R$. While the origin of such morphological transitions of the fatty acid self-assemblies is not clear from SANS data, molecular dynamic simulations can provide detailed insight into the assembly process (discussed below).

2.4. Molecular Dynamic Simulations. The addition of the counterion (ethanolamine) drives a morphological change in the self-assembled state of fatty acid onto $m$SiO$_2$ nanoparticles. We use molecular dynamics (MD) simulations to understand the mechanism of self-assembly of fatty acid molecules on the surface of $m$SiO$_2$. All simulations were performed using GROMACS 4.6.3$^{41}$ and visualized in VMD. In our simulations, the amount of fatty acid was kept constant, and the counterion molar ratio was systematically increased from $R = 0.1$ to 1.0. More details about the simulation setup are shown in Table S1. In a typical simulation run, a mixture of unionized (protonated) fatty acid and deprotonated fatty acid with protonated counterion molecules corresponding to different $R$ values was randomly placed above the $m$SiO$_2$ surface. The mixture together with the $m$SiO$_2$ surface was solvated in a water box using the TIP3P model.$^{43}$ Energy minimization followed by 500-ps NVT pre-equilibration using
Apart from the shape, the mean size of surface assemblies and line. The foam stability parameter for change, the electrostatic interaction \(47\) (understand the driving force that triggers the morphological transition of fatty acid molecules on the particle surface. To understand the driving force that triggers the morphological change, the electrostatic interaction \(47\) \(e_{\text{elec}}\) between fatty acid and mSiO\(_2\) and the van der Waals interaction \(E_{\text{vdW}}\) among fatty acid alkyl chains at different R values are calculated and shown in Figure 4d,e, respectively. At \(R < 0.2\), a small fraction of fatty acid molecules exist in the deprotonated state and adsorb onto mSiO\(_2\) by an electrostatic attraction. In our simulations, we find that at \(R = 0.1\), the fatty acid assembly is composed of 4 deprotonated fatty acid molecules and 66 fatty acid molecules, and the weakly negative-charged portions of the surface aggregate serve as adsorption sites, immobilizing the bulky assembly at the positive-charged sites. At \(R > 0.2\), an increasing number of deprotonated fatty acid molecules are bound to mSiO\(_2\) via an electrostatic attraction (red spheres in Figure 4a). At \(R = 0.5\), the number of deprotonated fatty acid molecules is equal to that of protonated fatty acid molecules. The electrostatic interaction between fatty acid and mSiO\(_2\) and the van der Waals attraction between the hydrocarbon chains of the molecules are both significant. Therefore, small fatty acid assemblies comprising both protonated and deprotonated fatty acid molecules are adsorbed onto the mSiO\(_2\) surface where the deprotonated fatty acid molecules act as electrostatic linkers to mSiO\(_2\). For \(R > 0.7\), the majority of fatty acid molecules are present in their carboxylate forms. The mSiO\(_2\)-bound deprotonated fatty acid molecules first form a packed monolayer by the lateral organization of the alkyl chains via van der Waals attraction, and the excess deprotonated fatty acid molecules are then packed to the monolayer to form a thin bilayer. Thus, the increased \(E_{\text{elec}}\) between fatty acid assemblies and mSiO\(_2\) together with decreased \(E_{\text{vdW}}\) between fatty acid molecules drives the morphological transition of fatty acid assembly from a large patch to a thin bilayer upon increasing \(R\). These observations on the morphological transition of fatty acid molecules on mSiO\(_2\) nanoparticles with increasing \(R\) agree with the SANS experiments (see section 2.3).

2.5. Foam Stability in Fatty Acid–mSiO\(_2\) Aqueous Solution. The foam stability of fatty acid soaps in aqueous solution is known to be related to the morphology of fatty acid assemblies at the air–water interface. However, the origin of...
superior foam observed in mixtures of oppositely charged nanoparticles and amphiphiles is not well understood. Here, we aim to interrelate the state of fatty acid assemblies formed on mSiO2 nanoparticles with their ability to stabilize the air–water interface (i.e., foam). The stability of foams formed by the mixture of fatty acid and mSiO2 with increasing R was tested at pH 6. A typical foaming experiment was performed using an aqueous mixture of 0.02 M fatty acid and 1.0 wt % mSiO2 with increasing R from 0.0 to 1.0. The used concentration of fatty acid was equivalent to $\Gamma_{\text{max}}$ at R = 1.0. The foam was produced from the fatty acid and mSiO2 mixture by vigorous shaking, and it was kept undisturbed at room temperature for 18 h. The change in the foam volume of the mixture after 18 h is monitored using digital imaging as shown in Figure 5a. The stability of the foam produced by the fatty acid–mSiO2 mixture at a given R is quantified using a foam stability parameter, $S$, represented as $S = \frac{v_{\text{final}}}{v_{\text{initial}}}$ where $v_{\text{initial}}$ and $v_{\text{final}}$ are the volumes of foam immediately after shaking and after 18 h of equilibration, respectively. For R = 0, the foam stability parameter was equal to zero since no foam could be produced from the pure fatty acid and mSiO2 mixture without a counterion (Figure 5a,b). By adding a small amount of counterions (R = 0.05), S increased from 0 to 0.7. By further increasing R, S reached a plateau value around 0.8 from R = 0.2 to 0.5. For R > 0.5, S decreased to a final value of 0.2 at R = 1 (Figure 5b). From these results, we define three regions of foam stability. Region I corresponds to low foam stability for $0 < R < 0.05$. Region II, 0.05 < R < 0.5, corresponds to high foam stability. Region III also corresponds to a low foam stability regime for 0.5 < R < 1.0. We further investigate the origin of change in foam stability with increasing R by microscale imaging of the bubbles in all three identified regions for $R = 0.05, 0.2$, and 1.0 (Figure 5c–e). In region I, the bubbles were spherical, highlighting the large interfacial tension between air and water. Transforming from region I to region II, the shape of bubbles undergoes a change from smooth sphere to rippled nonspherical. This change in the shape of the bubble upon increasing R can be attributed to the adsorption of the fatty acid–mSiO2 complex at the air–water interface and corresponding interfacial jamming of the nanoparticles. We believe that the adsorption of fatty acid patches onto mSiO2 makes the nanoparticles partially hydrophobic, driving its adsorption onto the air–water interface. Following such interfacial adsorption, the shape transformation of the bubbles is driven by two key factors: (a) jamming of nanoparticles in the thin films between the bubbles upon liquid drainage hindering the relaxation of the bubbles to spherical shape; and (b) compression of liquid films by nanoparticle jamming causing the buckled and rough appearance of the bubble surface. Furthermore, we observe that the shape of bubbles recovers to a smooth sphere from rippled perturbed shape upon increasing R to 1.0 (region III). It should be noted that no foam could be formed by mixture of mSiO2 and the counterion, highlighting the critical role of fatty acid in the foaming process (Figure 5b, squares).

In region I, only a few patches of fatty acid molecules are present at the mSiO2 surfaces (sections 2.3 and 2.4), which induce enough amphiphilicity to adsorb at the air–water interface. Therefore, hydrophilicity and weak amphiphilic characters of the nanoparticles in region I resulted in the lack of foam stability. In region II, the number of fatty acid patches at the particle surface was enough to reach an appropriate contact angle value, which leads to the adsorption of particles at the air–water interface. The patchy particles formed a dense layer at the interface protecting the bubbles against coalescence and coarsening due to jamming phenomenon, thus leading to the observed stable foams. In the region III, the fatty acid formed a continuous bilayer structure on the mSiO2 nanoparticle surface, leading to hydrophilic surface and diminishing the interfacial activity of the fatty acid-nanoparticle complex. This lack of interfacial activity of fatty acid–nanoparticle complex destabilizes the air bubbles and leads to poor foam stability (sections 2.3 and 2.4). Thus, the fatty acid–mSiO2 nanoparticles stay in the liquid phase and sediment to the bottom of solution due to the fatty acid-mediated heteroaggregation of the mSiO2 nanoparticles (Figure 5a,e). This absence of nanoparticles at the air–water interface spontaneously drives the bubble coalescence, drainage, and coarsening without any physical or energetic barrier(s). These foaming experiments highlight a direct relationship between the fatty acid structure on mSiO2 and their interfacial property. We find that patches of fatty acid on mSiO2 nanoparticles are necessary for increasing the interfacial activity of the complex and enhancing the corresponding foam stability. We show that the self-assembled state of fatty acid molecules on mSiO2 directs the interfacial activity of the composite nanostructure and the resulting macroscopic properties such as foam stability. The strong correlation between the self-assembled state of fatty acid molecules on the surface of mSiO2 nanoparticles and foam stability leads to the formation of programmable foams for which the stability can be tuned by modifying R.

3. CONCLUSIONS

This study presents the effect of the counterion-to-fatty acid molar ratio, R, on the self-assembled state of fatty acid molecules on aminopropyl-modified silica nanoparticles. We show that the maximum amount of fatty acid that can be adsorbed on the mSiO2 increases with increasing R. The increase in the amount of fatty acid molecules adsorbed on positively charged mSiO2 nanoparticles (at pH 6) is driven by an increase in the number of negatively charged deprotonated fatty acid molecules upon increasing R. The increase in the maximum surface excess of fatty acid on mSiO2 with increasing R drives a morphological change in the self-assembled state of fatty acids at the nanoparticle surface from discrete patches to the continuous layer. The control over that morphological state of fatty acid on mSiO2 by changing R enables programming the hydrophilic/hydrophobic characteristics of the fatty acid–mSiO2 nanoparticle complex. At low R, the fatty acid molecules form large discrete patches on the surface of mSiO2, which decompose and spread on mSiO2 to form a continuous layer at high R, evidenced by the analysis of SANS profiles and MD simulations. This morphological change is induced by the increased electrostatic interaction between fatty acid and mSiO2 along with the decreased van der Waals interaction between fatty acid molecules upon increasing R. The self-assembled state of fatty acid on the surface of mSiO2 is strongly correlated with the interfacial activity of the complex. We demonstrate that the foam stability of the mixture can be directed by altering the adsorbed state of the fatty acid molecules onto mSiO2 by changing the counterion-to-fatty acid molar ratio. This study provides a fundamental basis to comprehend the nontrivial effects of counterions on morphological evolution and phase transition of fatty acid assemblies formed on nanoparticles. Further work on such modified silica nanoparticle and their dispersion with fatty acid
can facilitate new principles of designing ultrastable foams valuable in cosmetics and food industries.52,53

**ASSOCIATED CONTENT**

1 Supporting Information

The Supporting Information is available free of charge at https://pubs.acs.org/doi/10.1021/acs.langmuir.0c00156.

Characterization of silica nanoparticles using SAXS and zeta potential-pH titration, amount of undissolved fatty acid at different R values, surface tension calibration curve, surface tension of fatty acid at R = 0, surface area-to-volume ratio determined by Porod’s analysis of SANS profile, derivation of raspberry model under core contrast matched condition, and MD simulation setup (PDF)

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Notes

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