Erratum: “Measurement of HDCO/H2CO Ratios in the Envelopes of Extremely Cold Protostars in Orion” (2015, ApJ, 814, 31)

Miju Kang1,2,3, Minho Choi1, Amelia M. Stutz4, and Ken’ichi Tatematsu5,6

1 Korea Astronomy and Space Science Institute, 776 Daedeokdaero, Yuseong, Daejeon 305-348, Korea; mjkang@kasi.re.kr
2 Korea University of Science and Technology, Daejeon 305-350, Korea
3 Max-Planck-Institut für Radioastronomie, Auf dem Hügel 69, 53121 Bonn, Germany
4 Max Planck Institute for Astronomy, Königstuhl 17, D-69117 Heidelberg, Germany
5 National Astronomical Observatory of Japan, 2-21-1 Osawa, Mitaka, Tokyo 181-8588, Japan
6 Department of Astronomical Science, The Graduate University for Advanced Studies (SOKENDAI), 2-21-1 Osawa, Mitaka, Tokyo 181-8588, Japan

Received 2017 January 4; published 2017 February 14

1. Source Identification

It was found that there are inconsistencies of sources ID numbering between our paper and Furlan et al. (2016). This problem affects only the first column of Table 1 and only the five rows that have both HOPS and PBRS IDs. We provide here the updated Table 1 with the HOPS IDs given by Furlan et al. (2016).

Table 1
List of Observed Sources

| Sourcea | R.A.  | Decl.  | Tb bol | Lbol | Field |
|---------|-------|--------|--------|------|-------|
| Sourcea | (h:m:s) | (°: ′′: ′′) | (K) | (Le) |       |
| HOPS ID | PBRS ID |
|---------|---------|
| 405     | 119019  | 05:40:58.4 | −08:05:36.1 | 34 | 1.6 | L1641 |
| 169     | 05:36:36.0 | −06:38:54.0 | 35 | 4.5 | L1641 |
| 398     | 082005  | 05:41:29.4 | −02:21:17.1 | 29 | 1.0 | NGC 2024 |
| 400     | 090003  | 05:42:45.2 | −01:16:14.2 | 36 | 2.7 | NGC 2024 |
| 358     | 05:46:07.2 | −00:13:30.9 | 44 | 30.6 | NGC 2068 |
| 373     | 05:46:30.7 | −00:02:36.8 | 36 | 5.2 | NGC 2068 |
| 403     | 093005  | 05:46:27.7 | −00:00:53.8 | 31 | 1.7 | NGC 2068 |
| 359     | 05:47:24.8 | 00:20:58.2 | 39 | 12.6 | NGC 2068 |
| 341     | 05:47:00.9 | 00:26:20.8 | 36 | 3.6 | NGC 2068 |
| 404     | 097002  | 05:48:07.7 | 00:33:50.8 | 33 | 1.1 | NGC 2068 |
| 354     | 05:54:24.1 | 01:44:20.2 | 37 | 7.5 | L1622 |

| Sourcea | R.A.  | Decl.  | Tb bol | Lbol | Field |
|---------|-------|--------|--------|------|-------|
| Sourcea | (h:m:s) | (°: ′′: ′′) | (K) | (Le) |       |
| Non-PBRS |       |       |       |      |       |
| 164     | 05:37:00.5 | −06:37:10.5 | 50 | 0.6 | L1641 |
| 297     | 05:41:23.3 | −02:17:35.8 | 46 | 1.0 | NGC 2024 |
| 321     | 05:46:33.2 | 00:00:02.2 | 74 | 4.6 | NGC 2068 |
| 360     | 05:47:27.1 | 00:20:33.1 | 36 | 2.2 | NGC 2068 |

Notes.

a In case there are two source IDs, we use the PBRS ID in the text.
b Uncertainties of Tb bol and Lbol are ∼15% (Stutz et al. 2013).
c Tb bol and Lbol of non-PBRSs are from A. Stutz (2015, private communication) and Furlan et al. (2016).

Reference

Furlan, E., Fischer, W. J., Ali, B., et al. 2016, ApJS, 224, 5
Stutz, A. M., Tobin, J. J., Stanke, T., et al. 2013, ApJ, 767, 36
MEASUREMENT OF HDCO/H2CO RATIOS IN THE ENVELOPES OF EXTREMELY COLD PROTOSTARS IN ORION

Miju Kang1,2,3, Minho Choi4, Amelia M. Stutz5, and Ken’ichi Tatematsu5,6
1 Korea Astronomy and Space Science Institute, 776 Daeedokdae-ro, Yuseong, Daejeon 305-348, Korea; mjkang@kasi.re.kr
2 Korea University of Science and Technology, Daejeon 305-350, Korea
3 Max-Planck-Institut für Radioastronomie, Auf dem Hügel 69, D-53121 Bonn, Germany
4 Max Planck Institute for Astronomy, Königstuhl 17, D-69117 Heidelberg, Germany
5 National Astronomical Observatory of Japan, 2-21-1 Osawa, Mitaka, Tokyo 181-8588, Japan
6 Department of Astronomical Science, SOKENDAI (The Graduate University for Advanced Studies), 2-21-1 Osawa, Mitaka, Tokyo 181-8588, Japan

Received 2015 July 23; accepted 2015 October 12; published 2015 November 13

ABSTRACT

We present observations of HDCO and H2CO emission toward a sample of 15 Class 0 protostars in the Orion A and B clouds. Of these, 11 protostars are Herschel-identified PACS Bright Red Sources (PBRSs) and 4 are previously identified protostars. Our observations revealed the chemical properties of the PBRS envelope for the first time. The column densities of HDCO and H2CO are derived from single-dish observations at an angular resolution of ~20′ (~8400 AU). The degree of deuteration in H2CO ([HDCO]/[H2CO]) was estimated to range from 0.03 to 0.31. The deuteration fractionation of most PBRSs (70%) is similar to that of the non-PBRS sources. Three PBRSs (30%) exhibit high deuteration fractionation, larger than 0.15. The large variation of the deuteration fractionation of H2CO in the whole PBRS sample may reflect the diversity in the initial conditions of star-forming cores. There is no clear correlation between the [HDCO]/[H2CO] ratio and the evolutionary sequence of protostars.

Key words: astrochemistry – ISM: abundances – ISM: molecules – stars: formation

1. INTRODUCTION

Observing deuterated species is useful for probing the physical and chemical conditions of star-forming regions (Roberts & Millar 2000b; Caselli et al. 2002; Roueff & Gerin 2003; Crapsi et al. 2005; Tatematsu et al. 2010; Fontani et al. 2011; Caselli & Ceccarelli 2012; Sakai et al. 2012). The deuterium to hydrogen (D/H) ratio in the local interstellar medium is low, about 1.5 x 10−5, which is the D/H elemental abundance as predicted by the nucleosynthesis (Linsky 2003). By contrast, higher molecular D/H ratios have been observed from objects associated with star formation, such as molecular clouds (Loren & Wootten 1985; Turner 2001; Parise et al. 2009; Bergman et al. 2011), prestellar cores (Bacmann et al. 2003; Crapsi et al. 2005; Fontani et al. 2008), and protostellar cores (Ceccarelli et al. 1998; Loinard et al. 2002; Emprechtinger et al. 2009). Many observations and chemical models showed that deuterium-bearing molecules are enhanced during the cold prestellar core phase and released into the gas when a heating event, such as the formation of a protostar or the passage of a shock, evaporates the ice (Tielens 1983; Rodgers & Millar 1996; Ceccarelli et al. 2001; Bacmann et al. 2003; Maret et al. 2004; Caiazzo et al. 2011; Taquet et al. 2012; Awad et al. 2014; Fontani et al. 2014).

Formaldehyde (H2CO) is one of the key species in the synthesis of more complex organic molecules. The H2CO lines are ubiquitous in the interstellar medium and used to infer temperature and density of gas (Mangum & Wootten 1993; Ceccarelli et al. 2003). There have been debates on the dominant formation mechanism of deuterated H2CO: whether singly or doubly deuterated species (HDCO or D2CO) of formaldehyde form via active grain surface chemistry (Tielens 1983; Turner 1990; Ceccarelli et al. 2001; Loinard et al. 2001; Fontani et al. 2015) or gas-phase reactions (Langer et al. 1979; Roberts & Millar 2000a; Parise et al. 2009). Codega et al. (2012) investigated deuteration in the protostellar outflow shock of L1157-B1. They concluded that the measured deuteration fractionation provides a fossil record of the gas before it was shocked by the jet driven by the protostar. They noted that the deuteration ratios derived from the outer part of the L1157 dense envelope (L1157-B1) are smaller than the ratios derived from the IRAS 16293–2422 spectra that are close to the protostar, where the density is expected to be higher. Recently, high-resolution observations with a ~2″ resolution toward L1157-B1 showed that the emission of HDCO was detected mostly from the region of interface between the ambient material and the shock driven by active outflow from a low-mass Class 0 protostar L1157-mm (Fontani et al. 2014). A deuteration fraction [HDCO]/[H2CO] of ∼0.1 was measured in the HDCO emitting region. These observations confirmed that deuterated molecules are formed on the grain surface and released into gas phase by the shocks.

The Orion molecular cloud complex is one of the nearest active star-forming regions, positioned at a distance of ~420 pc (Hirotà et al. 2007; Menten et al. 2007; Kim et al. 2008). Stutz et al. (2013) discovered and characterized the PACS Bright Red Sources (PBRSs) in Orion. Selected to have extremely red 70–24 μm colors (log (λF(70 μm)/λF(24 μm)) ~ 1.65), the PBRSs have Tbol < 45 K and Lmm/Lbol > 0.6%. They are colder than the typical Class 0 protostars in Orion. Stutz et al. (2013) proposed that the PBRSs may be the youngest protostars identified and characterized to date, with relatively high envelope densities. The PBRSs are therefore ideal objects for investigating the earliest stage of protostellar evolution. The aim of this work is to investigate whether the youngest Class 0 objects, PBRSs, are different from non-PBRS Class 0 protostars by comparing the deuterated levels of H2CO.

In this paper, we report observations of selected protostars in the H2CO Jκ=2 → 1 transition and the HDCO Jκ=2 → 1 transitions with two
Table 1
List of Observed Sources

| HOPS ID | Sourcea | PBRS ID | R.A. (h:m:s) | Decl. (°: ′: ″) | \( T_{\text{bol}}^b \) (K) | \( L_{\text{bol}}^b \) (L\(_{\odot}\)) | Field |
|---------|---------|---------|-------------|----------------|----------------|----------------|-------|
| PBRSs   |         |         |             |                |                |                |       |
| 398     | 119019  | 05:40:58.4 | −08:05:36.1 | 34 | 1.6 | L1641 |
| 169     |         | 05:36:36.0 | −06:38:54.0 | 35 | 4.5 | L1641 |
| 400     | 082005  | 05:41:29.4 | −02:21:17.1 | 29 | 1.0 | NGC 2024 |
| 403     | 090003  | 05:42:45.2 | −01:16:14.2 | 36 | 2.7 | NGC 2024 |
| 358     |         | 05:46:07.2 | −00:13:30.9 | 44 | 30.6 | NGC 2068 |
| 373     |         | 05:46:30.7 | −00:02:36.8 | 36 | 5.2 | NGC 2068 |
| 404     | 093005  | 05:46:27.7 | −00:00:53.8 | 31 | 1.7 | NGC 2068 |
| 359     |         | 05:47:24.8 | 00:20:58.2 | 39 | 12.6 | NGC 2068 |
| 341     |         | 05:47:00.9 | 00:26:20.8 | 36 | 3.6 | NGC 2068 |
| 405     | 097002  | 05:48:07.7 | 00:33:50.8 | 33 | 1.1 | NGC 2068 |
| 354     |         | 05:54:24.1 | 01:44:20.2 | 37 | 7.5 | L1622 |
| Non-PBRSs |         |         |             |                |                |                |       |
| 164     |         | 05:37:00.5 | −06:37:10.5 | 50 | 0.6 | L1641 |
| 297     |         | 05:41:23.3 | −02:17:35.8 | 46 | 1.0 | NGC 2024 |
| 321     |         | 05:46:33.2 | 00:00:02.6 | 74 | 4.6 | NGC 2068 |
| 360     |         | 05:47:27.1 | 00:20:33.1 | 36 | 2.2 | NGC 2068 |

Notes.

a In case there are two source IDs, we use the PBRS ID in the text.
b Uncertainties in \( T_{\text{bol}} \) and \( L_{\text{bol}} \) are \( \sim 15\% \) (Stutz et al. 2013).
c \( T_{\text{bol}} \) and \( L_{\text{bol}} \) of non-PBRSs are from A. Stutz (2015, private communication) and E. Furfan et al. (2015, in preparation).

Table 2
Observed Transitions and Telescope Parameters

| Transition | Rest frequency (GHz) | \( A_{ul} \) (s\(^{-1}\)) | \( E_l \) (K) | \( \eta_{\text{hub}} \) | \( T_{\text{sys}}^e \) (K) |
|------------|----------------------|----------------|-------------|----------------|----------------|
| HDCO \( 2_0 \rightarrow 1_0 \) | 128.812865 | \( 5.4 \times 10^{-5} \) | 3.1 | 0.30, 0.33 | 240 |
| HDCO \( 2_1 \rightarrow 1_0 \) | 134.284909 | \( 4.6 \times 10^{-5} \) | 11.2 | 0.28, 0.31 | 230 |
| H\(_2\)CO \( 2_2 \rightarrow 1_1 \) | 140.839520 | \( 5.3 \times 10^{-5} \) | 15.2 | 0.25, 0.28 | 300 |

Note.

a Mean system temperature.

antennas of the Korean Very Long Baseline Interferometry Network (KVN) used in the single-dish mode. We describe source selection and the details of our KVN observations in Section 2. The main observational results are presented in Section 3. In Section 4 we derive the physical properties. In Section 5 we discuss the deuterium fractionation of protostars. A summary is given in Section 6.

2. SOURCE SELECTION AND OBSERVATIONS

The Herschel Orion Protostar Survey (HOPS) is a Herschel Open Time Key Program targeting about 300 Spitzer-identified protostars with PACS 70 and 160 \( \mu \)m photometry and a subset of 30 protostars with PACS spectroscopy (Fischer et al. 2010; Manoj et al. 2013; Stutz et al. 2013). Stutz et al. (2013) found 18 PBRS in the Orion molecular clouds using Herschel scanmap observations toward a subset of the HOPS fields. We selected 11 isolated PBRS that are situated away from other protostars to avoid confusion in the KVN beam (\( \sim 20'' \)). For comparison, we added 4 non-PBRS HOPS targets, located in the vicinity of the PBRS targets, to the sample. The non-PBRS targets were selected based on their bolometric temperature and distance to the PBRS targets. They are located in the L1641, NGC 2024, and NGC 2068 fields of Orion, where most of the PBRS targets are also located. The number of non-PBRS targets was limited by the available observing time. Both PBRS and non-PBRS targets are taken from the HOPS sample. The coordinates and physical parameters of the selected sources are listed in Table 1.

Observations were made with the KVN 21 m antennas in the single-dish telescope mode during the 2013 observing season, with the KVN Yonsei antenna at Seoul in 2013 September–October and the KVN Ulsan antenna in 2013 November–December. The telescope pointing was checked once every two hours by observing Orion IRc2 (Baudry et al. 1995) in the SiO v = 1 J = 1 \( \rightarrow 0 \) maser line and was good within \( \sim 5'' \). The antenna temperature was calibrated by the standard chopper-wheel method.

We used the spectrometer with a bandwidth of 64 MHz and 4096 channels, which gives a spectral channel width of 15.625 kHz. Table 2 lists the parameters of the observed lines. The spectrometer setting gives a velocity channel width of 0.036, 0.035, and 0.033 km s\(^{-1}\) for HDCO \( 2_0 \rightarrow 1_0,1_1 \), HDCO \( 2_1 \rightarrow 1_0,1_1 \), and H\(_2\)CO \( 2_2 \rightarrow 1_1 \), respectively. For all lines, Hanning smoothing was applied three times. The half power beam width is about \( 20'' \). Quantization correction factor (1.25) and sideband separation efficiency (0.8 for the KVN Ulsan...
129 GHz band) were applied to the KVN raw data. The data acquired in the antenna temperature scale, $T_A^*$, were converted to the main beam temperature scale, $T_{mb} = T_A^*/n_{mb}$, using the main beam efficiencies ($n_{mb}$) in Table 2. The data were processed with the GILDAS/CLASS software from Institut de Radioastronomie Millimétrique (http://www.iram.fr/IRAMFR/GILDAS).

3. RESULTS

The observed H$_2$CO $2_{1,2} \rightarrow 1_{1,1}$, HDCO $2_{0,2} \rightarrow 1_{0,1}$, and $2_{1,1} \rightarrow 1_{0,0}$ line spectra are shown in Figure 1 for PBRSs and Figure 2 for non-PBRSs. The results of the observations are summarized in Table 3, including integrated intensities, centroid velocities, and line widths derived by Gaussian fits to the spectra.

Figure 1. Spectra of the H$_2$CO $2_{1,2} \rightarrow 1_{1,1}$ transition, and the HDCO $2_{0,2} \rightarrow 1_{0,1}$ and $2_{1,1} \rightarrow 1_{0,0}$ transitions observed toward PBRS targets. Vertical dotted lines show the centroid velocities of the HDCO $2_{0,2} \rightarrow 1_{0,1}$ spectra. The green spectra are Gaussian fits. The orange spectra of HOPS 373 show individual components of the two-component Gaussian fit.
H$_2$CO $2_{1,2} \rightarrow 1_{1,1}$ emission was detected toward all targets. The line widths of all sources are smaller than 3 km s$^{-1}$. Two PBRS, 090003 and 097002, have quite small line widths, about 0.5 km s$^{-1}$. Several sources with relatively large line widths show flat top spectra, indicating either large optical depths or an overlap of multiple components. For example, the H$_2$CO spectrum of 090003 shows double peaks. Since the velocity of the central dip corresponds to the peak velocity of the HDCO $2_{0,2} \rightarrow 1_{0,1}$ spectrum, we prefer the interpretation of a large optical depth. HOPS 373 drives a CO outflow (Gibb & Little 2000), and the H$_2$CO spectrum shows broad-line wings extending to large velocities. For HOPS 373, we applied a two-component Gaussian fit and used the parameters derived from the narrow component, which allows us to focus on the emission arising from the envelope of the protostar.

HDCO $2_{0,2} \rightarrow 1_{0,1}$ emission was detected toward all sources. Line widths of the HDCO $2_{0,2} \rightarrow 1_{0,1}$ transition are narrower than those of the H$_2$CO $2_{1,2} \rightarrow 1_{1,1}$ transition. The narrow lines emitted by the deuterated formaldehyde suggest that the emission is optically thin and dominated by the cold outer envelopes of the protostars. HDCO $2_{1,1} \rightarrow 1_{0,0}$ emission was detected toward seven PBRSs. The qualities of the HDCO $2_{1,1} \rightarrow 1_{0,0}$ spectra toward 119019, 097002, and HOPS 354 are relatively poor. Spectral baselines (line free channels) of these sources seem to be worse than the other cases. The HDCO $2_{1,1} \rightarrow 1_{0,0}$ emission of 097002 may be a non-detection because the line is placed at a peak velocity slightly different from that of the other transitions detected toward this source.

4. ANALYSIS

4.1. H$_2$CO Column Density

We calculate the column densities of H$_2$CO. Assuming that the line is optically thin and that the source size is similar to the main beam size, the column density in a lower state (defined as energy level $u \rightarrow l = (J + 1)k_{a,k} + 1 \rightarrow Jk_{a,k}$) can be obtained.

![Figure 2. Same as Figure 1 but for non-PBRS targets.]

Table 3
Parameters of the Observed Spectra

| Source | $\int T_{mb} dv$ (K km s$^{-1}$) | $v_c$ (km s$^{-1}$) | $\Delta v$ (km s$^{-1}$) |
|--------|-----------------|-----------------|-----------------|
| 119019 | 3.07 ± 0.16     | 5.13 ± 0.04     | 1.74 ± 0.11     |
| HOPS 169 | 4.02 ± 0.16     | 6.99 ± 0.03     | 1.36 ± 0.06     |
| 082005 | 6.66 ± 0.10     | 9.66 ± 0.02     | 2.08 ± 0.04     |
| 090003 | 0.86 ± 0.05     | 8.42 ± 0.01     | 0.45 ± 0.02     |
| HOPS 358 | 7.27 ± 0.20     | 10.09 ± 0.03    | 2.21 ± 0.08     |
| HOPS 373 | 2.36 ± 0.13     | 10.28 ± 0.02    | 0.76 ± 0.04     |
| 093005 | 10.58 ± 0.15    | 10.23 ± 0.01    | 1.84 ± 0.03     |
| HOPS 359 | 6.28 ± 0.27     | 9.63 ± 0.04     | 2.12 ± 0.11     |
| HOPS 341 | 4.01 ± 0.12     | 9.67 ± 0.02     | 1.31 ± 0.05     |
| 097002 | 0.83 ± 0.04     | 9.58 ± 0.01     | 0.53 ± 0.03     |
| HOPS 354 | 6.03 ± 0.16     | 1.03 ± 0.03     | 2.58 ± 0.08     |
| HOPS 164 | 4.20 ± 0.13     | 5.84 ± 0.02     | 1.24 ± 0.04     |
| HOPS 297 | 4.07 ± 0.19     | 9.95 ± 0.05     | 2.33 ± 0.12     |
| HOPS 321 | 4.30 ± 0.16     | 10.22 ± 0.03    | 1.65 ± 0.08     |
| HOPS 360 | 4.64 ± 0.14     | 9.31 ± 0.03     | 1.98 ± 0.07     |

Note. The calibration uncertainty of 10% is not included (Lee et al. 2011).

* HOPS 373 shows an outflow feature. This table lists the parameters for the narrow component. The integrated intensity, centroid velocity, and line width for the line wing component are 13.31 ± 0.34 K km s$^{-1}$, 10.02 ± 0.09 km s$^{-1}$, and 7.75 ± 0.22 km s$^{-1}$, respectively.
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Table 4

| Source      | \(N(\text{H}_2\text{CO})\) \((10^{12} \text{ cm}^{-2})\) | \(N(\text{HDCO})\) \((10^{12} \text{ cm}^{-2})\) | [HDCO]/[H2CO] |
|-------------|-------------------------------------|-------------------------------------|----------------|
| 119019      | 11.7 ± 1.3                         | 0.79 ± 0.11                        | 0.07 ± 0.01    |
| HOPS 169    | 15.3 ± 1.6                         | 1.76 ± 0.26                        | 0.12 ± 0.02    |
| 082005      | 25.3 ± 2.6                         | 1.00 ± 0.19                        | 0.04 ± 0.04    |
| 090003      | 3.3 ± 0.4                          | 1.00 ± 0.15                        | 0.31 ± 0.06    |
| HOPS 358    | 27.6 ± 2.9                         | 2.33 ± 0.26                        | 0.08 ± 0.01    |
| HOPS 373    | 9.0 ± 1.0                          | 1.90 ± 0.25                        | 0.21 ± 0.04    |
| 093005      | 40.2 ± 4.1                         | 1.82 ± 0.23                        | 0.05 ± 0.01    |
| HOPS 359    | 23.9 ± 2.6                         | 2.61 ± 0.31                        | 0.11 ± 0.02    |
| HOPS 341    | 15.3 ± 1.6                         | 1.09 ± 0.14                        | 0.07 ± 0.01    |
| 097002      | 3.2 ± 0.4                          | 0.60 ± 0.12                        | 0.19 ± 0.04    |
| HOPS 354    | 23.0 ± 2.4                         | 1.65 ± 0.23                        | 0.07 ± 0.01    |
| HOPS 164    | 16.0 ± 1.7                         | 1.25 ± 0.18                        | 0.08 ± 0.01    |
| HOPS 297    | 15.5 ± 1.7                         | 1.00 ± 0.17                        | 0.06 ± 0.01    |
| HOPS 321    | 16.4 ± 1.7                         | 0.54 ± 0.10                        | 0.03 ± 0.01    |
| HOPS 360    | 17.6 ± 1.8                         | 1.52 ± 0.24                        | 0.09 ± 0.02    |

Note. The column densities are calculated assuming \(T_{\text{ex}} = 10\) K. The estimated errors come from the uncertainties of integrated intensities (Table 3), which include the statistical uncertainties and the calibration uncertainty of 10% (Lee et al. 2011).

by

\[
N_i = \frac{93.5 \times 10^3}{g_{\nu} A_{\nu 1}} \frac{1}{T_{\text{ex}}} \int T_{\text{mb}} \, dv, \tag{1}
\]

where \(h\) is the Planck’s constant, \(k\) is the Boltzmann’s constant, \(\nu\) is the frequency of the transition in GHz, \(T_{\text{ex}}\) is the excitation temperature, \(g\) is the statistical weight, \(A_{\nu 1}\) is the Einstein coefficient in s\(^{-1}\), \(\int T_{\text{mb}} \, dv\) is the integrated line intensity, and \(v\) is the velocity in km s\(^{-1}\) (Rohlfs & Wilson 1999). The column density is in cm\(^{-2}\), and the numerical factor in the equation corresponds to \(8\pi / c^3\) and a conversion factor, when it is expressed in the units given above. All parameters for molecules were taken from the JPL databases (Pickett et al. 1998).

The total column density of ortho-H2CO, \(N_{\text{ortho}}\), is related to the column density, \(N_i = N(J_{K_a K_c})\), in the lower state \(J_{K_a K_c}\) by

\[
\frac{N_{\text{ortho}}}{N(J_{K_a K_c})} = \frac{Z}{g(J_{K_a K_c})} \exp \left( \frac{E(J_{K_a K_c})}{kT_{\text{ex}}} \right), \tag{2}
\]

where \(g(J_{K_a K_c})\) is the statistical weight \(3(2J + 1)\) for ortho-H2CO, \(E(J_{K_a K_c})\) is the energy of a \(J_{K_a K_c}\) level, and \(Z\) is the partition function. If the molecules follow the Boltzmann distribution of a single \(T_{\text{ex}}\), the partition function is

\[
Z = \sum z = \sum g(J_{K_a K_c}) \exp \left( - \frac{E(J_{K_a K_c})}{kT_{\text{ex}}} \right). \tag{3}
\]

For ortho-H2CO, \(K_a\) can only be odd. The total H2CO column densities are calculated assuming an excitation temperature of 10 K and the statistical ortho to para ratio of 3:1 (Minh et al. 1995; Guzmán et al. 2013). The resulting column densities are given in Table 4. The column densities are not very sensitive to the assumed excitation temperature, when \(T_{\text{ex}} \gtrsim 10\) K (Roberts et al. 2002). Using an excitation temperature of 30 or 50 K changes the inferred column densities by a factor of about 2.2 or 3.7, respectively. For example, if we calculate column densities of H2CO adopting \(T_{\text{ex}} = 30\) K for 090003 and HOPS 341, their column densities become \(7.1 \times 10^{12}\) and \(33.0 \times 10^{12}\) cm\(^{-2}\), respectively. Indeed, we estimate \(T_{\text{ex}} \approx 14\) K from those sources with detections of both HDCO transitions (Section 4.3). Therefore, the assumption of \(T_{\text{ex}} = 10\) K is reasonable.

4.2. HDCO Column Density

HDCO is a nearly symmetric top molecule. Therefore, the treatment for calculating column density is similar to the case of H2CO. However, there is no H-pair, so there is no ortho/para modification. While H2CO has an electric dipole moment along the A axis only, HDCO has an extra dipole moment along the B axis. As a result, transitions between K ladders are allowed, and all K ladders are radiatively connected. HDCO lines have hyperfine structures (Langer et al. 1979). For the HDCO \(2_0,2 \rightarrow 1_0,1\) transition, the central group (2 components) dominates in intensity, and the velocity separation from the center to the satellites is \(<0.2\) km s\(^{-1}\). The hyperfine components are not expected to be resolved, but they can make the line look wide. For the purpose of column density calculations, we ignore the effects of hyperfine structure. We use \(\mu_i\) (2.324 Debye) for \(\mu_i\), since we are interested in the transitions in a K ladder (a type). The statistical weight \(g\) has a rotation contribution only, \(g(J_{K_a K_c}) = 2J + 1\). The HDCO transition is optically thin because deuterated species are 10–100 times less abundant than the main species.

The total HDCO column density is calculated by assuming an excitation temperature of 10 K and an optically thin line (Table 4). If we use \(T_{\text{ex}} = 30\) or 50 K, the HDCO column densities change by factors of about 3.4 or 6.7, respectively. The [HDCO]/[H2CO] ratios change by factors of about 1.6 or 1.8, respectively.

4.3. Excitation Temperature

We calculated the excitation temperature using the line ratio of the HDCO \(J_{K_a K_c} = 2_0,2 \rightarrow 1_0,1\) and \(2_1,1 \rightarrow 1_0,0\) transitions, assuming that they have the same excitation temperature. Because the \(J\) quantum numbers are the same, factors depending on \(J\) are common factors in calculating the column density ratio. The column density ratio, ignoring the common factors, is

\[
\frac{N_{2_0,2}}{N_{2_1,1}} = RT \frac{4}{3} \left[ 1 - \exp \left( -h\nu(2_0,2 - 1_0,1)/kT_{\text{ex}} \right) \right] \approx RT \frac{4}{3}, \tag{4}
\]

where \(RT = \int T_{\text{mb}}(2_1,1 - 1_0,0) \, dv / \int T_{\text{mb}}(2_0,2 - 1_0,1) \, dv\) is the line ratio. Because the frequencies are very similar, the right exponential factor after \(RT^4/3\) is nearly 1. The column density ratio should be the same as the ratio of partition terms, and here the statistical weight \(g\) cancels out since \(g\) only depends on \(J\).

\[
RT \frac{4}{3} = \exp \left( - \frac{E(1_0,0) - E(1_0,1)}{kT_{\text{ex}}} \right). \tag{5}
\]
is the peak temperature, and $E(l_{0,1})/k = 11.18297 \, \text{K}$ and $E(l_{0,1})/k = 3.09406 \, \text{K}$, the excitation temperature is,

$$T_{\text{ex}} = \frac{-8.09}{\ln(4/3RT)}.$$  \hspace{1cm} (6)

In our observations, seven sources are detected in both transitions. When the line ratio is close to $\sim 0.75$, $T_{\text{ex}}$ diverges. The excitation temperatures are summarized in Table 5. We obtained an average excitation temperature of $\sim 14 \pm 5 \, \text{K}$. Therefore, the $T_{\text{ex}} = 10 \, \text{K}$ used in the column density calculations is consistent with the measured $T_{\text{ex}}$.

4.4. Optical Depths and Line Widths

The assumption of an optically thin line is reasonable for the lines of the deuterated molecules based on their low abundances. However, the optical depth of the $H_2CO$ $2_{0,2} \rightarrow 1_{0,1}$ transition can be high because $H_2CO$ is abundant in molecular clouds. The optical depth of the $H_2CO$ line can be estimated by comparing the fluxes between $H_2CO$ and its isotopologue for the same transition. Unfortunately, our survey did not cover observations of the $H^13CO$ line. Though a direct measurement of the optical depth ($\tau$) is not available, we have roughly estimated the line optical depths using the solution of the line radiative transfer equation.

$$\tau = -\ln\left(1 - \left(T_{\text{peak}}/J_{\nu}(T_{\text{ex}}) - J_{\nu}(T_{\text{BG}})\right)\right),$$ \hspace{1cm} (7)

where $T_{\text{peak}}$ is the peak temperature, and $J_{\nu}(T_{\text{ex}})$ and $J_{\nu}(T_{\text{BG}})$ are the equivalent Rayleigh–Jeans excitation and background temperatures, respectively. The optical depths estimated in this way are between 0.3 and 1.9. In other studies, the optical depths of 0.4–1.1 were estimated from low-mass protostars (e.g., Maret et al. 2004) and $\sim 1.6$ from the dense core in the Horsehead PDR (Guzmán et al. 2011), based on the flux ratio of the $H_2CO$ and $H^13CO$ $2_{0,2} \rightarrow 1_{0,1}$ transition. Larger line width is also known to be coupled with larger line optical depth (Phillips et al. 1979; Roberts et al. 2002; Ceccarelli et al. 2003).

In Figure 3, we compare the line widths of $H_2CO$ $2_{0,2} \rightarrow 1_{0,1}$ and $HDCO$ $2_{0,2} \rightarrow 1_{0,1}$. Most sources with large $H_2CO$ line widths do not show a good agreement, which is likely due to the optical depth in the $H_2CO$ $2_{0,2} \rightarrow 1_{0,1}$ transition. Considering the optical depth of the $H_2CO$ estimated from our calculation, the column density of $H_2CO$ should be corrected by a factor of $\tau/(1 - \exp(-\tau))$, then $N(H_2CO)$ increases by a factor of 1.1 for $\tau = 0.3$ and 2.2 for $\tau = 1.9$.

5. DISCUSSION

5.1. Deuterium Fractionation

The last column of Table 4 lists $[HDCO]/[H_2CO]$ ratios calculated assuming $T_{\text{ex}} = 10 \, \text{K}$. This ratio is not very sensitive to $T_{\text{ex}}$ (Section 4.2). The $[HDCO]/[H_2CO]$ ratio ranges from 0.03 to 0.31, which is consistent with values derived from the low-mass Class 0 protostars by Parise et al. (2006). The average $[HDCO]/[H_2CO]$ ratio and standard deviation of the total target sample are 0.105 and 0.075, respectively. Figure 4(a) shows the distribution of the $[HDCO]/[H_2CO]$ ratios for the full sample. Considering that the ratio is always positive and that the distribution is asymmetric, the distribution can be characterized better with the mode rather than the average. The mode value and FWHM are $\sim 0.07$ and $\sim 0.02$, respectively. The $[HDCO]/[H_2CO]$ ratios of the three PBRSs on the high end (090003, HOPS 373, and 097002) are significantly larger than the mode value. They may represent either a long tail of a unimodal distribution or a secondary peak of a bimodal distribution. More extensive studies are necessary to understand the detailed shape of the distribution.

Figure 4(b) shows the $[HDCO]/[H_2CO]$ distributions for the PBRS and non-PBRS samples separately. About 30% of PBRSs (3/11) have high $[HDCO]/[H_2CO]$ ratios (>0.15), and 70% of PBRSs (8/11) have ratios similar to non-PBRSs. Both PBRSs and non-PBRSs have the same mode (0.07) as the full sample.

Since the number of non-PBRS sources is relatively small, the $[HDCO]/[H_2CO]$ ratios of Class 0 sources measured by Roberts et al. (2002) may be helpful in understanding the distributions. Figure 4(c) shows the $[HDCO]/[H_2CO]$ distribution of non-PBRS sources, including seven sources from Roberts et al. (2002). The general properties of the distribution

![Figure 3](image-url)
remain the same. The mode is ~0.07, and the range of values is less than ~0.12, which reinforces the finding that the PBRS distribution has a relatively large dispersion and that the three PBRSs on the high end are outliers. However, note that five sources in the sample of Roberts et al. (2002) are in regions closer than the Orion cloud, which could introduce some unexpected effects to the distribution. Therefore, a more extensive survey with a larger sample size will be helpful in understanding the distributions better.

Figure 5(a) shows a comparison of the [HDCO]/[H$_2$CO] ratios with and without optical depth correction. Although the optical depth corrections for the H$_2$CO observations make the [HDCO]/[H$_2$CO] ratios decrease for all sources, changes of the [HDCO]/[H$_2$CO] ratios are not much. In Figure 5(b), the overall distributions of the $\tau$-corrected [HDCO]/[H$_2$CO] ratios show similar characteristics compared with Figure 4(b). The three outliers with high deuterium fractionation are still far from the mode of the distribution. Even if we consider the optical depth, the [HDCO]/[H$_2$CO] ratios of 090003, HOPS 373, and 097002 are still high (>0.15). Therefore, in the subsequent discussions below, we will consider only the [HDCO]/[H$_2$CO] distribution derived with the assumption of optically thin lines.

The [HDCO]/[H$_2$CO] ratios are plotted against $T_{bol}$ and $L_{bol}$ in Figure 6. When plotted against $L_{bol}$ in Figure 6(b), no obvious correlation was found. The [HDCO]/[H$_2$CO] ratios for low-mass Class 0 protostars reported by Roberts et al. (2002) are also plotted in Figure 6(a). As suggested by Roberts et al. (2002), there is no marked correlation between the [HDCO]/[H$_2$CO] ratios and the bolometric temperature (a proxy of the evolutionary stage of protostars). Though the PBRS and non-PBRS samples show similar mode values, the PBRS sample shows a significantly larger scatter. This difference suggests that either PBRS have an intrinsically large variation in the deuterium fractionation or the three outliers are chemically distinct from the majority of Class 0 protostars.

5.2. Properties of the PBRS Sample

To focus on the large variation of the deuterium fractionation in the PBRS sample, we calculate the fractional abundances of the PBRS sample. The fractional HDCO and H$_2$CO abundances were calculated by dividing the total HDCO and H$_2$CO column densities by the H$_2$ column density i.e., X (HDCO) = [HDCO]/[H$_2$] and X(H$_2$CO) = [H$_2$CO]/[H$_2$]. Using the 870 $\mu$m flux density in Table 5 of Stutz et al. (2015), the beam-averaged column density of PBRS can be computed with:

$$N_{H_2} = \frac{F_\nu R}{B_\nu(T_B)\Omega \kappa_\nu \mu_m H},$$

where $\Omega$ is the beam solid angle, $\mu$ is the mean molecular weight of the interstellar medium, which we assume to be 2.8 (Kauffmann et al. 2008), $m_H$ is the mass of the hydrogen atom, $\kappa_\nu$ is the dust absorption coefficient (1.85 cm$^2$ g$^{-1}$, Schuller et al. 2009), and $R$ is the gas-to-dust mass ratio (assumed to be 100). We assume a dust temperature of 20 K (Stutz et al. 2010). The observed abundances of HDCO and H$_2$CO range from 2 $\times$ 10$^{-11}$ to 7 $\times$ 10$^{-11}$ and 8 $\times$ 10$^{-11}$ to 1 $\times$ 10$^{-9}$, respectively. The H$_2$CO abundances of PBRS are similar to the outer H$_2$CO abundances toward low-mass protostars reported...
by Maret et al. (2004). They have explained that the outer regions of the envelopes of Class 0 sources reflect the precollapse conditions based on the similarity of the values between the abundances of prestellar cores studied by Bacmann et al. (2002, 2003) and the outer H$_2$CO abundances of low-mass protostars.

The HDCO and H$_2$CO abundances relative to H$_2$ are plotted in Figure 7. As the H$_2$CO abundance increases, the HDCO abundance increases for the PRRS with the ratio of >0.1. The highly deuterated PRRSs (HDCO/[H$_2$CO] > 0.15) are significantly different from the other PRRSs in that they have small H$_2$CO abundances and their H$_2$CO line widths are quite narrow (<1 km s$^{-1}$, Figure 3). The degree of deuterium fractionation is suggested to increase with increasing CO depletion (Bacmann et al. 2003). The CO and H$_2$CO molecules are depleted by a similar factor in the outer envelope of Class 0 protostar (Maret et al. 2004). The low H$_2$CO abundance of highly deuterated PRRS is likely to be explained by the depletion of H$_2$CO. The narrow line widths imply that these cores are quiescent, which is associated with early phases of core evolution. Therefore, the PRRSs with high [HDCO]/[H$_2$CO] ratios are probably in the very earliest stage of star formation.

Figure 8 shows the relation between [HDCO]/[H$_2$CO] and the mass-to-luminosity ratio that is expected to decrease with time. The PRRSs with high [HDCO]/[H$_2$CO] ratios have relatively large mass-to-luminosity ratios, indicating that they are likely in the earliest stage of star formation. However, two PRRSs with the largest mass-to-luminosity ratios have low [HDCO]/[H$_2$CO] ratios. Therefore, it is difficult to find a simple relation between the two quantities. If the mass-to-luminosity ratio is a good tracer of evolution, [HDCO]/[H$_2$CO] seems to have a large dispersion at early stages and converge to a typical value of Class 0 sources at later stages.

The large variation of deuterium fractionation in the whole PRRS sample leads us to suggest that the PRRSs form in diverse conditions or have diverse formation histories. Indeed, the degree of deuterium fractionation of H$_2$CO is sensitive to the initial D/H ratios of gaseous molecules determined before the collapse phase (Turner 1990; Charnley et al. 1992; Roberts et al. 2002; Cazaux et al. 2011; Aikawa et al. 2012).

Figure 6. [HDCO]/[H$_2$CO] ratios of PRRSs (open circle) and non-PRRSs (filled circle) plotted against (a) the bolometric temperature and (b) the luminosity. Blue square symbols represent the low-mass protostellar cores of Roberts et al. (2002). The dashed line shows the canonical $T_{bol}$ division between the Class 0 and I sources (Chen et al. 1995).

Figure 7. Abundance ratios of H$_2$CO and HDCO relative to H$_2$ molecules for the PRRS sample. The gray dashed lines represent the ratios of 1.0 and 0.10 from top to bottom. Three highly deuterated PRRS are located on the left side of the blue solid line representing the ratio of 0.15.

Figure 8. [HDCO]/[H$_2$CO] ratios plotted against the mass-to-luminosity ratios for the PRRS sample.
PBRS 097002 and 090003 are among the highly deuterated PBRSs and have flat visibility amplitude profiles in the 2.9 mm dust continuum observations by Tobin et al. (2015). They interpret that the PBRSs with flat visibility amplitude profiles are the youngest in a brief phase of high infall/accretion. Since PBRSs 093005 and 082005 have the lowest [HDCO]/[H$_2$CO] ratios and also have flat visibility amplitude profiles, it is unclear if the variation of deuterium fractionation in H$_2$CO is due to the core evolution. Additional observations in pure gas-phase species, e.g., N$_2$D$^+$ and NH$_3^+$, can help our understanding of the chemical evolutionary sequence of PBRSs.

6. SUMMARY

We observed 15 Class 0 protostars (11 PBRS and 4 non-PBRS) in the Orion molecular cloud complex using the KVN in the single-dish telescope mode. The chemical properties of PBRSs were investigated in the H$_2$CO $2_{1,2} \rightarrow 1_{1,1}$, HDCO $2_{0,2} \rightarrow 1_{0,1}$, and $2_{0,2} \rightarrow 1_{0,1}$ lines. The main results are summarized as follows.

1. The H$_2$CO $2_{1,2} \rightarrow 1_{1,1}$ and HDCO $2_{0,2} \rightarrow 1_{0,1}$ emission lines were detected toward all targets. The HDCO $2_{1,1} \rightarrow 1_{0,0}$ emission line was detected toward seven PBRSs.

2. The [HDCO]/[H$_2$CO] ratio ranges from 0.03 to 0.31. The deuterium fractionation of most PBRSs (70%) is similar to that of non-PBRS Class 0 protostars, and three PBRSs (30%) have significantly high deuterium fractionation, greater than 0.15. These findings hint that the deuterium fractionation of PBRSs may have a distribution that is different from that of non-PBRSs, but future studies with larger sample sizes are needed to reach a statistically more significant conclusion.

3. The high [HDCO]/[H$_2$CO] ratios of the three PBRSs imply that they are in the earliest phase of the star formation. The large variation of deuterium fractionation in the whole PBRS sample suggests that PBRSs form in diverse conditions of temperature and/or density, because [HDCO]/[H$_2$CO] ratios are usually interpreted as a fossil memory of the earlier, colder phase of star formation.

4. No clear correlation between the deuterium fractionation of H$_2$CO and the evolutionary state of cores could be found. Further studies in various molecules are needed to investigate the difference between evolutionary sequence and the initial conditions of the PBRS samples.

We thank Friedrich Wyrowski, Thomas Megeath, Bérengère Parise, Jeong-Eun Lee, and Karl M. Menten for helpful discussions.

REFERENCES

Aikawa, Y., Wakelam, V., Hersant, F., Garrod, R. T., & Herbst, E. 2012, ApJ, 760, 40

Awad, Z., Viti, S., Bayet, E., & Caselli, P. 2014, MNRAS, 443, 275

Baumann, A., Le floch, B., Ceccarelli, C., et al. 2002, A&A, 389, L6

Bacmann, A., Le floch, B., Ceccarelli, C., et al. 2003, ApJL, 585, L55