Scanpaths in reading are informative about sentence processing

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ABSTRACT
Scanpaths, sequences of fixations of the eyes, have historically played an important role in eyetracking research but their use has remained highly limited until recently. Here, we summarize earlier research and argue that scanpaths are a valuable source of information for reading research, specifically in the study of sentence comprehension. We also discuss a freely available, open source scanpath analysis method that we used to evaluate theoretical claims about human parsing and about how the parser guides the eyes during reading. This scanpath analysis is shown to yield new information that was missed when traditional approaches were used to study theories about eye guidance during garden-pathing. We also show how relatively subtle scanpath effects can be detected when we report the scanpath analysis of a large eyetracking corpus. In sum, we argue that scanpath analyses are likely to serve as an increasingly important tool in reading research, and perhaps also in other areas where eyetracking is used, e.g., in studies using the visual world paradigm.

KEYWORDS: scanpaths, reading, eye movements, parsing.
1 Introduction

Over the last decades, eyetracking has been established as one of the most important tools for studying human language processing. Eyetracking studies contributed to the investigation of the lexical retrieval of words and the processing of syntax, semantics, and discourse. The two dominant experimental paradigms that have been used are reading studies and visual world studies. In reading studies, the movements of the eyes are recorded as sentences are read. Typical dependent variables are word-based duration measures such as the time the eyes dwell on a word before proceeding to the next word or the probability to move backwards from a word (regression probability). Increased dwell times and rates of regressions on a particular word are commonly interpreted as reflecting difficulty to process that word or one of the previous words (Rayner, 1998; Clifton et al., 2007; Vasishth et al., 2012). In visual word experiments, participants hear recordings of sentences while watching visual scenes. Typically, a scene is displayed in which one object is a target that is mentioned in the sentence; other objects serve as distractors. The amount of looks to the target object and their timing can uncover when various types of information come into play during comprehension (Huettig et al., 2011). For instance, if the target word is a pronoun ("him" vs "her"), the speed at which people converge with their gaze to the visual representation of the antecedent of the pronoun and the proportion of looks to distractors can be informative about the mechanisms underlying reference resolution (e.g., Kaiser et al., 2009).

Common to all these approaches is the fact that they considerably reduce the recorded information about eye movements. In reading studies, a word or small region is singled out for which a duration measure or a regression probability is computed, that is, the measure is aggregated across trials and participants. Eye movements that occurred before the eyes entered this region and after they left it are discarded. This approach is entirely reasonable if the effect of the experimental manipulation is focused to a particular critical region and if the effect of the manipulation is expected to be largely the same in all participants. In many cases, these assumptions may be reasonable; in this paper, however, we argue that they can be problematic in certain important situations. The issue is not limited to reading studies; information may be similarly lost in analyses of data acquired in visual world experiments. Eye movements in this type of experiment are most often evaluated using the percentage of looks to a region in the visual stimulus (target or distractor) as a function of time. This involves aggregating the data of all trials in a condition and the individual fixation sequences are lost. If there were several qualitatively different fixation patterns, reflecting different cognitive processes, these would not be identifiable in the aggregate. The purpose of these simplifications of the eyetracking data is (i) to get rid of irrelevant variance which could mask the effects of interest and (ii) to extract a dependent measure that can be analyzed using standard statistical tools. Clearly, simplification of the data is a trade-off: the raw data is difficult to interpret but an over-simplified signal can be misleading.

In this paper, we will focus on eye movements in reading and show that some theoretically important eye movement phenomena are not captured by the traditional eyetracking measures. These measures can therefore be misleading in some circumstances. In recent work, we introduced a new method for analyzing eye movements that addresses some of the issues with traditional measures. We will explain which problem exactly this method aims to solve and how the method works. Next, we will discuss how we used this method in (i) a reading experiment and (ii) an analysis of a large-scale eyetracking corpus. Before we start to describe this new method, it is useful to have a closer look at the data we are dealing with.
1.1 Eye movements in reading: What do they look like?

In this paper, we discuss our analyses of two sets of eyetracking data (these analyses are reported in von der Malsburg and Vasishth, 2012; von der Malsburg et al., 2012). The first data set was collected in a reading experiment that investigated the processing of Spanish garden-path sentences (von der Malsburg and Vasishth, 2012). The 70 Spanish native speakers tested in this study came from a relatively homogeneous population and the experimental sentences all followed a particular syntactic construction (average number of words: 18.5). Because of a temporary attachment ambiguity of an adverbial clause these sentences were somewhat difficult to process, but they still constitute an easy type of garden-path sentence. The design of the study resembles that of typical reading studies in sentence processing research: the conditions were minimally different from each other, the sentences had comparable length, and the presentation of items (pseudo-randomly intermixed with fillers) was counterbalanced in the standard manner. The second data set is the Potsdam Sentence Corpus (henceforth, the PSC), a database of eye movements recorded from 230 participants reading a set of 144 sentences (Kliegl et al., 2004). The participants ranged from teenagers to pensioners and came from diverse socioeconomic backgrounds. The sentence material consisted of simple German sentences (ranging from 5 to 11 words, average: 7.9) that were designed to represent a large variety of syntactic constructions. Thus, the PSC can be regarded as a representative sample of how the general population reads common sentence types.

How would a machine direct its eyes when reading a sentence? One obvious strategy would be to scan the words from left to right one at a time, looking on each word until it is fully processed and to move to the next when finished. The spatial pattern of fixations generated by such a reader would not be interesting because it would always be the same regardless of the sentence being read: a monotonic movement in one direction. All information about the underlying processes would be conveyed by the temporal dynamics. While human readers use a similar reading strategy, the targets of their saccades are far from being as predictable as those of our hypothetical reading machine. In the PSC, for instance, 19% of the saccades skip the next word (skipped words are typically short and have high frequency), 17% of the saccades result in another fixation on the current word, and 14% of the saccades are directed at previous words. Hence, only 50% of the saccades target the next word in the sentence. This means that even when people read simple sentences that do not pose any larger difficulties, they deviate considerably from a monotonous left-to-right reading style. Several factors have been shown to causes these deviations from a straight eye movement trajectory. They include oculo-motor constraints, lexical processing, and higher-level language processing (Rayner, 1998; Bicknell and Levy, 2011).

Fig. 1 shows eye movements from the PSC that were recorded when participants read the sentence in (1). This sentence has long words (easy to target) and canonical word order (easy to process). Of all sentences in the PSC, this one elicited the most regular reading patterns. The scanpaths in fig. 1 can therefore be seen as marking the lower bound on irregularity in scanpaths. Although the participants read this sentence mostly from left to right, the plot shows that in almost all trials words were skipped and that in several trials material was revisited.

(1) Wolfgang’s Töchter studieren Literatur und Maschinenbau.

When a sentence contains words that are difficult to integrate into the syntactic or semantic
Figure 1: Eye movement as recorded in 24 trials in which participants read the sentence “Wolfgang’s daughters study literature and engineering.” Each panel shows how a specific participant read the sentence. Words are on the x-axis, time is on the y-axis, and the lines show the trajectory of the eyes. In only three trials (7, 17, 20), the eyes proceeded strictly from word to word. In most trials the short word “and” was skipped. In several trials the eyes returned to earlier material (1, 3, 4, 21, 22, 26).

interpretation of the sentence, reading patterns can deviate even more from a straight unidirectional reading pattern. Quite early in psycholinguistic research, Frazier and Rayner (1982) demonstrated that encountering the disambiguating word in a garden-path sentence such as (2) can cause multi-fixation regressive eye movements which they interpreted as reflecting syntactic reanalysis. For instance, when reading the sentence in (2), readers have a tendency to interpret the noun phrase “the sock” initially as the object of “mending”. However, when “fell” is encountered, it becomes clear that this role assignment cannot be maintained and the interpretation of the sentence has to be revised.

(2) While Mary was mending the sock fell off her lap.

At the time when Frazier and Rayner carried out their study, no statistical tools were available for analyzing the fixation patterns that ensued when the critical word was read. Therefore, they analyzed the data qualitatively. Later studies used quantitative measures to confirm that syntactic reanalysis causes complex regression patterns but the precise nature of these patterns could not be resolved (Meseguer et al., 2002; Mitchell et al., 2008). To illustrate what kind of data the authors of these studies were dealing with we selected 24 representative trials from an experiment that we conducted to investigate the same questions as those that Frazier and Rayner pursued (von der Malsburg and Vasishth, 2012). These trials are shown in fig. 2. In
Figure 2: Eye movement as recorded in 24 trials in which participants read the sentences in (3) (“El profesor dijo . . .”). Each panel shows how a specific participant read the sentence. Words are on the x-axis, time is on the y-axis, and the lines show the trajectory of the eyes.

about 50% of the trials, the participants of this experiment produced regressive eye movements after they read the critical word in the sentence showing that sentence processing can have a dramatic impact on the gaze trajectory. In the vast majority of cases, these regressive eye movements consisted of several fixations, which rules out a trivial numerical representation of the gaze trajectory. The measures devised by earlier authors (Meseguer et al., 2002; Mitchell et al., 2008) reduced these fixation sequences (the scanpaths) to only the first backwards directed saccade following the fixation on the critical word. The benefit of this approach is that the distribution of landing sites of this saccade can be modeled using standard statistical tools; the drawback is that information about eye movement events following this first regressive saccade is lost. One goal of this paper is to show that this loss of information can have a critical impact on the inferences drawn from eye movement data.

Summarizing this section, we can say that, despite the linear nature of text, reading patterns are quite complex, and that they may contain important information about the cognitive processes underlying reading. The next section will describe a method that can be used to leverage that information.

2 Analyzing Scanpaths

The central problem when analyzing eye movement patterns (scanpaths) is that they are complex. A scanpath can consist of an arbitrary number of fixations and these fixations are described in three dimensions: two spatial dimensions (e.g. coordinates on the screen) and time (duration of a fixation). When we analyze traditional measures such as the first pass reading time of a word, we can compare all measurements by simply calculating their differences and
we can calculate means, standard deviations, and confidence intervals to make inferences. In contrast to that it is unclear how two measurements should be compared if they consist of scanpaths. What is the mean of a set of scanpaths and how can we describe the variance? These questions could be answered if there was a vector representation of scanpaths in a common vector space but deriving such a representation is not trivial due to the variable length of scanpaths ranging from two fixations to an unbounded number of fixations. One way to derive a vector representation has been proposed by Josephson and Holmes (2002). The procedure is as following: calculate all pair-wise similarities of the scanpaths in a data set. Next, set up an $n$-dimensional vector space and for each scanpath randomly place a vector in this space. Then, use an iterative procedure that optimizes the positions of these vectors until their distances in the vector space approximate the previously calculated similarities of the corresponding scanpaths as well as possible (this procedure is called non-metric multidimensional scaling, Kruskal, 1964). These vector representations—we call them maps of scanpath space—have various desirable properties: scanpaths that are similar are located close to each other in the vector space and dissimilar scanpaths are far apart. This property allows us to apply clustering procedures to the map of scanpaths in order to identify categories of scanpath patterns. We can also calculate the variance in the scanpaths, identify an "average" scanpath (i.e., the scanpath in the center of gravity of a set), and locate the areas of highest density in order find scanpath patterns that occurred often.

The missing ingredient for these things to work is an appropriate similarity measure that captures the relevant properties of scanpaths. One proposal has been to use the Levenshtein distance (Brandt and Stark, 1997; Salvucci and Anderson, 2001) which quantifies the (dis)similarity of two sequences of symbols as the number of edit-operations that have to be performed on one sequence to transform it into the other (Levenshtein, 1966). These operations are deletion and insertion of a symbol and substitution of a symbol by another symbol. This measure can be applied to eye movements in the following way: partition the visual stimulus into regions and uniquely label each region with a letter. A sequence of fixations can then be represented by a sequence of letters in which the $n$-th letter specifies the location of the $n$-th fixation (see fig. 3 for an illustration).

The Levenshtein metric has many desirable properties such as the ability to deal with sequences of unequal length and being relatively cheap to compute. However, it also has some important limitations. First, reading times are ignored completely because they are not part of the representation on which the Levenshtein metric operates (strings of letters). So whether a fixation in one scanpath that is not present in the other is long or short does not have any impact on the similarity score for these two scanpaths. The second limitation is that the similarity of two fixation sequences depends on how the visual stimulus was partitioned. If the regions are large, the scanpaths in a data set will on average be more similar to each other than when they are small because the probability that fixations coincide in the same region is higher if these regions are large. What is a reasonable partitioning? In reading, words serve reasonably well as regions of interest but there is no general answer to this question. The third limitation of the Levenshtein metric is that a deviation between two scanpaths in one fixation leads to an increase of the dissimilarity of 1 irrespective of whether the deviation is spatially large or small. That means that if a fixation in one scanpath is on a word and the corresponding fixation is not on the same word but really close, the two fixations will be counted as being as dissimilar as two

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1The Needleman-Wunsch algorithm is commonly used to do the computation and takes processing time and memory resources proportional to the product of the lengths of the two sequences (Needleman and Wunsch, 1970).
The Scasim measure

Our measure uses the same general approach as the Levenshtein distance. The difference is the way we account for deviations in two scanpaths. Where the Levenshtein distance assigns a “cost” of 1 for every fixation that differs in two scanpaths, we assign a cost that is a function of the spatial locations and the fixation durations: if a fixation has to be deleted in one scanpath, the cost for that deletion is the duration of that fixation. Deleting a long fixation therefore leads to a larger overall dissimilarity between two scanpaths than deleting a short fixation. Similarly, the cost of inserting a fixation is simply the duration of the inserted fixation. The cost for substituting one fixation by another fixation depends on the durations and locations of the
two fixations. If they have the same location, the cost of the substitution is simply the difference in their fixation durations. If the two fixations are extremely far apart, the cost is given by the sum of the fixation durations. There are two reasons for this choice. First, if the two fixations are long, this means that the spatial deviation between them is temporally longer and should therefore lead to increased overall dissimilarity. Second, this choice means that substituting two fixations that are extremely far apart amounts to the same dissimilarity as deleting one of the fixation and inserting the other. This property avoids discontinuities in the similarity function, e.g., when the duration of one fixation converges to zero. What is the dissimilarity when the two fixations are neither at the same location nor extremely far apart, i.e., if they are only somewhat spatially separated? In this case, the cost of the substitution is a weighted sum of the difference of the fixation durations and the sum of the fixation durations. The weights are a function of the spatial distance and are determined by a function that mimics the exponential drop in visual acuity of human vision (Daniel and Whitteridge, 1961; Rovamo et al., 1978).

Some useful properties of the resulting similarity measure that follow from these definitions are: (i) Partitioning of the stimulus in more or less arbitrary regions is not necessary because the measures is a continuous function of the coordinates and durations of the fixations in two scanpaths. (ii) The measure is theory-agnostic, i.e., it does not make any assumptions about the significance of certain types of eye movements, e.g., a regression in reading is not treated any different than any other eye movement pattern. (iii) Similarity scores can be efficiently computed with a variant of the Needleman-Wunsch algorithm (Needleman and Wunsch, 1970). See von der Malsburg and Vasishth (2011) for a detailed discussion of Scasim. See fig. 3 for an illustration showing how the similarity of two scanpaths is computed with Scasim.

There is not one true similarity measure for scanpaths and our measure constitutes only one possible way to quantify differences between scanpaths. What’s similar and what’s not really depends on the question being asked and while our measure may be useful in one type of analysis it may not be suitable in other types. Given that, it is not surprising that quite a few other similarity measures have recently been proposed which all have different properties and applications (Salvucci and Anderson, 2001; Cristino et al., 2010; Jarodzka et al., 2010; Mathôt et al., 2012; Coco and Keller, 2012). Unfortunately, there is no space here to describe these measures, but some are discussed and compared with Scasim in von der Malsburg and Vasishth (2011).

The next sections will describe two different ways in which we used the Scasim measure to analyze eye movements in reading.

3 Case study 1: Regression patterns during reanalysis

In von der Malsburg and Vasishth (2011, 2012) we investigated scanpaths in response to the disambiguation of Spanish garden-path sentences such as (3) (adapted from Meseguer et al., 2002).

(3) El profesor dijo que los alumnos se levantarán ... 
The teacher said that the students had to stand up ...

a. [AdvC cuando los directores entraron en la clase].
   [AdvC when the directors came into the classroom].

b. [AdvC cuando los directores entraran en la clase].
   [AdvC when the directors come into the classroom].
Sentences (3a) and (3b) contain an adverbial clause (“cuando los directores . . .”) which can initially be attached to the main verb of the sentence (“dijo”) or to the embedded verb (“levantaran”). The correct attachment site is only determined when the verb of the adverbial phrase is read (“entraron” / “entraran”) because the mood of this verb (indicative or subjunctive) agrees with either the main verb or the embedded verb. Low attachment to the embedded verb is preferred in Spanish in agreement with the late-closure principle (Frazier, 1979). Therefore the sentence processor experiences difficulty at “entraron” in (3a) because this word indicates that the initial attachment was incorrect. A revision of the attachment has to be carried out. In sentence (3c), the attachment is unambiguously clear at all times because the “si”-clause can only attach to “levantaran”.

The main question that we investigated was: which strategy does the parser use to revise the interpretation of the sentence? Three hypotheses about the mechanisms underlying revision have been proposed in the literature (see Frazier & Rayner, 1982, for a detailed discussion). The forward reanalysis hypothesis states that reanalysis is carried out by means of normal parsing routines. The parser is assumed to return to the beginning of the sentence and to re-parse the sentence while looking for choice points at which the misanalysis can be prevented. The backward reanalysis hypothesis states that the parser switches to reverse gear, undoing parsing decisions word-by-word until the crucial choice point is reached (Kaplan, 1972). The selective reanalysis hypothesis posits that the parser intelligently identifies the problem and that it deploys targeted repair mechanisms (Frazier and Rayner, 1982). Under the additional assumption that the eyes are tightly coupled to the sentence processor (the eyes look at the word that is currently being processed; Just and Carpenter, 1980) these hypotheses afford clearly distinguishable predictions about scanpath patterns. According to forward reanalysis, the eyes should return to the beginning of the sentence and start a second pass over the material so far. According to backward reanalysis, the eyes should reverse the direction going backwards until the beginning of the ambiguous region is reached (“cuando”) and should then switch back to normal forward operation. According to selective reanalysis, the eyes should perform targeted saccades to words that are affected by the reanalysis: the ambiguous region, the main, and the embedded verb.

To test for these patterns, we recorded eye movements from 70 participants who read sentences as in (3). Since no reanalysis is required in (3b) where the critical word (“entraran”) only supports the preferred interpretation, any regressive scanpath patterns that occur more often in (3a) than in (3b) can be interpreted as reflecting reanalysis. Thus, one way to address the question about reanalysis strategies is to perform a cluster analysis of scanpath patterns with the goal to identify qualitatively different types of scanpaths and to see if one or several of these types occur more often in condition (3a) than in (3b).

### 3.1 Analysis

The complete analysis was carried out in GNU-R (R Development Core Team, 2009). We first extracted from all trials regressive scanpaths that occurred after the critical word was read. Next, we used our Scasim measure to calculate the pair-wise similarities of all these regression patterns. This can be done with a function called Scasim which is freely available from the authors.\(^2\) This function takes a data frame (basically a table) as input which contains,\(^2\)http://www.ling.uni-potsdam.de/~malsburg
Figure 4: Three projections of the 7-dimensional map of scanpaths calculated for the analysis of scanpaths recorded in our Spanish experiment. Each point is a scanpath. The colors indicate membership to the three clusters (A, B, C) that were identified in the cluster analysis.

chronologically ordered, a line for every fixation in the data set. One column identifies the trial to which a fixation belongs, other columns specify the x and y coordinates and the duration of a fixation. The resulting matrix of similarity scores was then used to fit a map of scanpath space, i.e., a n-dimensional vector space with a vector for each regressive scanpath (see fig. 4). This was done using the function isoMDS from the package MASS which performs multidimensional scaling. Once the vector representation of scanpaths is available, a large range of statistical methods can be used to analyze the variance in scanpaths. We chose mixture of Gaussian modeling for the cluster analysis. Mixture models describe the distribution of data points using a set of multivariate Gaussians each of which represents one cluster. One important benefit over other clustering procedures, such as k-means, is that mixture models can identify overlapping clusters based on their distributional properties. The parameters of the Gaussians (position, spread, orientation) were calculated using expectation maximization (package mclust, Fraley and Raftery, 2002, 2007). A Bayesian information criterion was used to determine the optimal number of clusters (Schwarz, 1978).

The cluster analysis identified three broad classes of scanpath patterns which can be seen in the map of scanpaths in fig. 4. What scanpath pattern do these classes represent? A distribution of reaction times can be characterized by calculating its mean. Similarly we can characterize a cluster by identifying its center of gravity (the mean of the multivariate Gaussian). The scanpaths that are closest to that center can be seen as being prototypical for that cluster. Fig. 5 shows one prototypical scanpath for each of the three clusters that we found. In one pattern (A), the eyes reread the sentence as predicted by the forward reanalysis hypothesis. In another pattern (B), the eyes returned from the disambiguating region (“entraron/entraran”) to the ambiguous region. In the third pattern (C), the eyes returned from the spill-over region (“en la clase”) to the disambiguating region.

Pattern A (rereading) occurred more often in sentences as in (3a) in which the preferred interpretation is invalidated, suggesting that rereading reflects a reanalysis strategy. It was also found that readers with high working memory capacity produced this pattern more often than readers with a low working memory score. In the context of other results obtained in
Figure 5: Prototypical scanpaths for three clusters identified in the cluster analysis of the scanpaths recorded in our Spanish study. These scanpaths were located at the center of gravity of the three clusters shown in fig. 4. In A, the eyes returned to the beginning of the sentences after having read the disambiguating word in region 8 and then reread the sentence. In B, the eyes rapidly regressed from the disambiguating word to the ambiguous region 7. In C, the eyes returned from the spill-over region 9 to the disambiguating region.

that study, this was interpreted as showing that high-capacity readers commit more eagerly to an attachment decision—and consequently have to revise these decisions more often—than low-capacity readers who were hypothesized to leave the attachment occasionally unspecified in order to preserve resources. Pattern C (revisiting the disambiguating word) occurred equally often in the temporarily ambiguous conditions (3a,b) but less often in the unambiguous condition (3c). The difference between sentences in conditions (3a) and (3b) was only one letter (“entraron” vs. “entraran”) and it seems likely that type C regressions served to increase the certainty about what has been read in cases where the targeted word was decisive for the attachment of the adverbial clause (c.f. Bicknell and Levy, 2010). See von der Malsburg and Vasishth (2012) for more details.

Various aspects of these results suggest that analyses of scanpath patterns can contribute substantially to the interpretation of eyetracking data. We will briefly discuss two ways in which an analysis of traditional eyetracking measures would have missed important information in the eyetracking record.

First, Meseguer et al. (2002) found a high rate of regressions from the postdisambiguation region to regions close to the beginning of the sentence in an experiment that used almost the same sentences as ours. Their study also found that these regressions occurred more often in the garden-path condition. Meseguer and colleagues suspected that these regressions were targeted at the main verb of the sentence (“dijo”) which was the true attachment site in these sentences and therefore argued in support of selective reanalysis which predicts these eye movements. However, examining scanpaths in cluster A (rereading), shows that regions close to the beginning of the sentence were often used as a stepping-stone on the way to the first word. This suggests that the main verb may not have been the actual target of regression triggered by disambiguation; rather, saccades to the main verb may have been the result of an undershoot on the way to the first word where rereading was initiated. This shows that the functional
interpretation of saccades analysed in isolation can be problematic and it shows that scanpath analyses can help to avoid misinterpretations.

Second, working memory was found to modulate the rate of pattern A scanpaths (rereading) and pattern B scanpaths (regressions to the disambiguating region). However, the effects were different for these two types of scanpaths. There was no effect of working memory on the rate of pattern C scanpaths (revisiting the disambiguating region). A traditional regression measure such as regression probability conflates these effects by aggregating across the three functionally different types of scanpaths. The resulting pattern of effects is difficult to interpret. Indeed, if only regression probability were to be analyzed in the above case, qualitatively different effects of working memory on scanpaths may cancel each other out so that no influence of working memory would be detected at all. This shows that separating qualitatively different eye movement phenomena can in some situations reveal effects that would otherwise go unnoticed.

4 Case study 2: Scanpath variance in general reading

Our scanpath analysis of regressions in response to garden-pathing has shed new light on the mechanisms underlying the processing of ambiguous material. Can scanpaths also be informative about other processes involved in reading? One way to answer this question empirically is to analyze a database containing eye movements for a variety of constructions (e.g., the Potsdam Sentence Corpus, PSC) and to investigate the factors that influence scanpaths. These factors may include oculo-motor, sentence processing constraints, and individual difference in readers. In von der Malsburg et al. (2012), we reviewed the literature and identified three variables that should influence scanpath patterns. The effects of these variables have previously only been shown using simplifying, word-based eyetracking measures such as regression probability. The first variable is the syntactic processing difficulty of a sentence. In a wide range of studies, it has been found that if a word is difficult to integrate with the sentence fragment read so far, the result is often an increased rate of regressive eye movements (see Clifton et al., 2007, for a review). The second variable influencing scanpaths is the length of words. The literature on oculo-motor control in reading has found that short words are skipped more often (Brysbaert and Vitu, 1998; Kliegl et al., 2004; Drieghe et al., 2005) and that the eyes often return to skipped words (Vitu and McConkie, 2000; Engbert et al., 2005). The third variable is the age of readers: older readers skip words more often and also regress more often than young readers (Kliegl et al., 2004; Rayner et al., 2006). The effects of all three variables have also been documented for the PSC (Kliegl et al., 2004; Boston et al., 2008).

The goals of our scanpath analysis of the PSC were two-fold: First, we wanted to validate our scanpath measure. If the measure does what it is supposed to do, it should recover the scanpath effects that the literature hinted at. Analyzing the PSC can be seen as a particularly hard test because, as we reported above, the sentences were easy and the eyes went relatively straightforwardly from left to right; in other words, the scanpath effects in the PSC are presumably relatively subtle. The second goal of this study was to model, for the first time, the joint effects of the three variables, which had been studied in separate research fields (research on sentence processing, oculo-motor control, and cognitive aging), and their interactions.

In contrast to the scanpath analysis of syntactic reanalysis, we were not interested in identifying categories of scanpaths but in the degree to which the eyes deviate from a regular reading pattern. This irregularity of the scanpath can be quantified on the basis of maps of scanpaths similar to those described above. We used a similar procedure to calculate 144 of these maps, one for each of the 144 sentences in the PSC. Each of the 230 points on a map represents how
one of 230 readers read the sentence. Fig. 6 shows the maps for the following two sentences:

(4) *Wolfgang's Töchter studieren Literatur und Maschinenbau.*

Wolfgang's daughters study literature and engineering.

(5) *Den Ton gab der Künstler seinem Gehilfen.*

The artist gave the clay to his apprentice.

‘The artist gave the clay to his apprentice.’

The first sentence has canonical word order and long words. Hence, it should elicit relatively regular scanpaths. The second sentence has non-canonical word order, contains a lexical ambiguity (“Ton” can mean clay or sound), and has short words, which should result in relatively irregular scanpaths. Looking at the maps in fig. 6, we see that the density of scanpaths is higher for the first sentence and lower for the second sentence. This follows from the fact that scanpaths for sentence (4) were more similar to each other than those recorded for sentence (5) (distance on the map reflects dissimilarity according to our Scasim measure). Thus we can use density on the map to quantify the regularity of scanpaths: if a scanpath is located in a low-density area of a map it is relatively irregular (i.e., there were few similar scanpaths). If, however, a scanpath is located in a high-density area it followed a common pattern and more regular pattern.
In order to calculate density, we again used mixture models, this time however to derive a density function for each of the 144 maps. The density scores of the scanpaths were then modeled as a function of syntactic difficulty of sentences, average word length in sentences, age of readers, and the interactions of these factors (linear mixed models, Bates, 2005). Syntactic difficulty was measured as the average surprisal (Hale, 2001) and the average retrieval cost in a sentence Lewis and Vasishth (2005). Surprisal quantifies the unexpectedness of a word given the preceding words and retrieval cost the difficulty of retrieving dependents of a word from working memory assuming temporal decay and similarity-based interference between memory items. These two measures thus capture different aspects of sentence processing. Both measures were taken from Boston et al. (2011) and added to the model as separate predictors.

All predictions were confirmed. Older readers produced more irregular scanpaths than younger readers. Sentences with short words, high surprisal, or high retrieval cost elicited more irregular scanpath patterns. Additionally, both syntactic measures interacted with age to the effect that older readers had weaker effects of syntax than younger readers. The results thus show that our scanpath measure is sensitive to effects attributable to different levels of processing. Also, they show that scanpath analyses can be informative not only when the effects are relatively pronounced, as typically seen in garden-path sentences, but also when the eyes move relatively straight from left to right, that is, when the effects are relatively subtle.

How would an analysis based on traditional eyetracking measures have fared? We have not done a formal comparison but it is easy to see how, for instance, an analysis of regression probability could be problematic: a short word length and a high syntactic difficulty both increase the rate of regressions and therefore increase irregularity. The type of regression may be different, though. In the case of word length, we expect a regression back to the skipped word directly following the skip. Thus, at the short word the eyes hit a snag but that leads only to a small detour in the gaze trajectory. In the case of a syntactic obstacle, the detour may be larger—perhaps the eyes revisit earlier material for rereading? Syntax may therefore have a different impact on scanpaths than word length. Yet, this difference would not be reflected in regression probability. Of course, the difference in this particular example can be captured in other measures, e.g., total reading time, but these measures will fail to distinguish other patterns. Thus, classical eyetracking measures present a puzzle that is difficult to solve. Compared to that, our scanpath metric is a compound measure of all aspects in a scanpath. All spatial and temporal deviations from a regular reading pattern are captured and distinguishable.

5 Conclusions

Scanpaths have been in the focus of pioneering eyetracking studies in the research on reading (Frazier and Rayner, 1982) and visual scene perception (Yarbus, 1967). Nevertheless, analyses of scanpaths have not gained much traction, perhaps because of a lack of suitable methods for analyzing them. Particularly in reading research, scanpaths have not played an important role. Here, we summarized our previous work showing that scanpaths are analytically tractable and informative about the processes involved in reading. It remains to been seen how the proposed methods can be applied to other types of data such as eye movements in the visual world paradigm.
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