Electrical control of spin dynamics in finite one-dimensional systems

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We investigate the possibility of the electrical control of spin transfer in monoatomic chains incorporating spin-impurities. Our theoretical framework is the mixed quantum-classical (Ehrenfest) description of the spin dynamics, in the spirit of the s-d-model, where the itinerant electrons are described by a tight-binding model while localized spins are treated classically. Our main focus is on the dynamical exchange interaction between two well-separated spins. This can be quantified by the transfer of excitations in the form of transverse spin oscillations. We systematically study the effect of an electrostatic gate bias \( V_g \) on the interconnecting channel and we map out the long-range dynamical spin transfer as a function of \( V_g \). We identify regions of \( V_g \) giving rise to significant amplification of the spin transmission at low frequencies and relate this to the electronic structure of the channel.

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I. INTRODUCTION

The rapid development of the field of spintronics\textsuperscript{11} over the past two decades has uncovered exciting and novel phenomena related to the dynamics of the electronic spin in a wide variety of systems, ranging from bulk materials to spatially-confined structures.\textsuperscript{3} Fueled by the ever-growing needs for speed, capacity and energy-efficiency in computing, the central objective in understanding and ultimately controlling the spin properties in the solid state has been constantly shifting towards the nano-scale. At these lengths and times the conventional methods for spin control, based on magnetic fields alone, are limited by scalability issues. Alternative approaches are thus sought and they typically involve electric fields of some form.\textsuperscript{4}

One way to manipulate spins by purely electrical means relies on the spin-transfer torque mechanism.\textsuperscript{5} This approach uses spin-polarized currents to control the direction of the magnetization and has been realized in various nanostructured materials ranging from magnetic multilayers\textsuperscript{6} to, more recently, single atoms in STM-type geometries.\textsuperscript{7} Alternative to electric current control is the optical control, such as in the laser-driven ultrafast magnetization switching.\textsuperscript{8} In a somewhat different context, the optical manipulation of single spins in bulk media\textsuperscript{9} is at the heart of the most promising candidates for the quantum information processing technology.\textsuperscript{10,11}

Another alternative is based on the idea of an electrostatic control of the spin-density, i.e. of the construction of spin-transistor type devices.\textsuperscript{10,11} Recently, the concept of gate-modulated spin-pumping\textsuperscript{12} transistors has been studied theoretically in infinite graphene strips with patterned magnetic implantations.\textsuperscript{13} Importantly, such devices rely on the efficient transport of spin information between two points in space and time, and require the possibility to actively tune the propagating spin-signal during its transport. In this work we explore this possibility for atomistic spin-conductors. We consider a finite mono-atomic wire linking two localized spin-carrying impurities. When one of the localized spins is set into precession, it generates a perturbation in the spin-density. This perturbation is carried through the wire by conducting electrons and can be detected in the dynamical response of the second spin. We show that the propagation of the spin-signal and consequentially the dynamical communication between the two spin centers, can be tuned by means of an electrostatic gate applied to the interconnecting wire. Our main finding is an enhancement of the communication for a certain range of gate voltages. This is linked to the modification of the electronic structure of the wire induced by the applied electrostatic gate.

Because of their considerable size the systems investigated here are still beyond the present numerical capabilities of first-principles dynamics and as such they are described by model Hamiltonians. Usually the dynamics is approached within the linear response approximation.\textsuperscript{14} In this paper we go beyond the linear response limit and propose a fully microscopic description based on the time-dependent Schrödinger equation, which allows us to describe arbitrary excitations. In other words our simulations are not limited to small gate voltages or small-angle spin precession. We use a single-band tight-binding Hamiltonian to model the itinerant s-electrons in our metallic wires and include local Heisenberg interactions to a number of magnetic ions (typically one or two). The latter are modeled as classical spin degrees of freedom and enter on equal footing in the common mixed quantum-classical dynamic portrait of the system.

This paper is organized as follows. In Section II we introduce the model system and our theoretical framework. Section III contains the results of our investigation. Firstly we investigate the electron response of an atomic wire, not including magnetic impurities, to local spin excitations. Secondly, we study the dynamical interplay between two spin impurities electronically connected by the wire and show how such a dynamics is affected by the gate voltage. Finally we draw some conclusions.
II. THE MODEL

A cartoon of the device considered is presented in Fig. 1. This consists of an $N$-sites long atomic wire interconnecting two magnetic centers. The latter, represented in the figure by the spin-vectors, enter our model as substitutional magnetic impurities positioned at the two ends of the wire (the local spin originates from the deeply localized $d$-electrons). One of them, say the left-hand side spin-center $S_1$, is labeled as “driven”, as its precession is induced and sustained by a local (at that site) magnetic field. The other localized spin, $S_2$, located at the other end of the chain is the “probe” spin and it is not directly coupled to any external magnetic field but only to the electron gas. In this way $S_2$ probes the magnetic excitations produced by the driven spin $S_1$ as these propagate through the interconnecting wire. The device is described as a mixed quantum-classical system in the spirit of the (s-d)-model, where the time-dependent Hamiltonians of the two exchange-coupled spin sub-systems read

$$
\hat{H}_{el}(t) = \sum_{i,j}^{N} H_{ij}^{TB} c_i^\dagger c_j + \sum_{\alpha=1}^{N} \epsilon_i c_i^\dagger c_i - J \sum_{\alpha,\beta=1}^{2} \left[ S_1(t) c_1^\dagger c_1 + S_2(t) c_N^\dagger c_N \right] \cdot \hat{\sigma}^{\alpha\beta},
$$

where $H_T^{TB} = \varepsilon_i \delta_{ij} + \gamma \delta_{i,i+1}$ is a single-orbital tight-binding Hamiltonian with on-site energies $\varepsilon_i$ and hopping integral $\gamma$ ($\gamma$ sets the relevant energy scale for the entire system); $c_i^\dagger (c_i)$ is the creation (annihilation) operator for an electron with spin-up ($\alpha = 1$) or spin-down ($\alpha = 2$) at the atomic site $i$; $\hat{\sigma}^{\alpha\beta} = \frac{i}{2}(\sigma_x, \sigma_y, \sigma_z)$ is the electron spin operator, $\{\sigma_i\}_{i=x,y,z}$ being the set of Pauli matrices; $S_{1,2}$ is the unit vector in the direction of the localized spin; $J > 0$ is the exchange coupling strength.

The classical dynamics of the local spins is governed by $H_S(t)$, which describes the interaction of $S_{1,2}$ with the mean-field local electron spin-density $s_i \equiv \langle \hat{\sigma} \rangle_i$, taken as the instantaneous expectation value of the conduction-electron spin at site $i$ (see further in text for the exact definition). The classical Hamiltonian also includes interaction with the external magnetic field $B = (0, 0, B_z)$, which is applied locally to $S_1$ only, in order to drive its precession. We further assume $g = 2$ for the localized spins and $\mu_B = 5.788 \times 10^{-5}$eV/T is the Bohr magneton.

In order to study the dynamics of this system in the time-domain we integrate the coupled quantum and classical equations of motion (EOM) of the two spin subsystems using the fourth-order Runge-Kutta (RK4) algorithm. As a result the set of trajectories for the local electronic spin-densities $s_i(t)$ are obtained as well as those of the driven and the probe classical spins $S_{1,2}(t)$. The typical length of the chain that we consider is $N = 100$.

The effect of an electrostatic gate is incorporated in our model as a rigid shift of the onsite energies $\varepsilon_i \rightarrow \varepsilon_i + V_g$, where $i \in [i_1, i_2]$ is a certain range of sites in the middle of the chain and $V_g$ is the gate voltage.

![FIG. 1: (Color online) Model system investigated in this work: two localized spins are electronically connected by a monatomic atomic wire, where electrons can flow. An electrostatic gate is applied to some of the interconnecting sites.](image)
III. DYNAMICS OF THE ITINERANT SPINS WITH FROZEN IMPURITIES

A. No external gate

As a preliminary step towards the combined quantum-classical dynamics we first address the dynamics of the spin-density of the itinerant electrons in the presence of the two local spins, whose directions are fixed, e.g. $S_{1,2}|\hat{z}\rangle$. A spin excitation is produced by a small but finite spatially-localized perturbation in the spin-density. As initial density matrix at $t_0$ we use the one that corresponds to a perturbed Hamiltonian $\hat{H}_g(t_0 - \delta t)$ in which one of the localized spins is slightly tilted in the $x-z$ plane, such that $\mathbf{S}_1(t_0 - \delta t) \cdot \hat{z} \approx \theta \hat{z}$, $\theta \leq 5^\circ$. However at $t_0$ we bring $\mathbf{S}_1$ back to its original direction (||$\hat{z}$) where it stays throughout the simulation. In other words we study the time evolution of the system with the two local spins parallel to each other starting from the ground state electronic charge density of the system where one of the two spins is tilted by a small angle.

The evolution of the density matrix for $t > t_0$ is obtained by
\[
\hat{\rho}(t) = e^{-iH_{el}t/\hbar} \hat{\rho}(t_0) e^{iH_{el}t/\hbar},
\]
which translates into the following expression for the density matrix elements
\[
\rho_{kl}^\sigma(t) = \sum_{mn} e^{-i\omega_{mn}t} c_{km}^\sigma c_{ln}^{\sigma^*} \sum_{ij} c_{im}^{\sigma^*} c_{jn}^\beta \rho_{ij}^{\sigma\beta}(t_0).
\]
(5)

In Eq. (5) we have defined the frequencies $\omega_{mn} \equiv e_m - e_n$ corresponding to differences between the eigenvalues $e_m$ of $\hat{H}_g(t_0)$. The coefficients $c_{km}^\sigma = \langle k\sigma | \varphi_m \rangle$ are the projections of the eigenvectors $|\varphi_m\rangle$ on the spin-resolved atomic orbital basis $|k\sigma\rangle \equiv |k\rangle \otimes |\sigma\rangle$, where $k$ represents the atomic site and $\sigma = \uparrow, \downarrow$ is the spin component.

The typical evolution of the spin density of the itinerant electrons resulting from excitation described above is presented in Fig. 2. The trajectories of the individual on-site spin polarizations $\Delta s_i^z(t) = s_i^z(t) - s_i^z(t_0)$ stemming from Eq. (5) are perfectly identical (on the scale of the graph) to those obtained by the numerical integration of the EOMs and directly from Eq. (5). Fig. 2 demonstrates that this finite 1D model atomic system is a relatively efficient waveguide for spin wave-packets (of sub-femtosecond duration) at least over the investigated time-scales of a few picoseconds.

![FIG. 2: (Color online) Spin excitation of one dimensional wire.](image-url)

(b) Initial spin-polarization $s^z(t_0)$ as a function of site index. (c) Time and space evolution of $\Delta s^z_k$ with the color shade representing the magnitude of absolute value of $\Delta s^z_k(t)$. Note that $2\tau$ is the wave-packet round-trip time as also seen in the bottom panel.

Eq. (5) can also be used to calculate directly the spectra of particular spin observables. These match perfectly with those calculated by performing the discrete Fourier Transform (dFT) of the time-dependent spin-densities obtained over the finite duration of the dynamic simulation. Clearly, in the absence of the localized impurities (i.e. for a finite homogeneous tight-binding chain) $\omega_{mn}$ can be calculated exactly. The spectrum of $\Delta s^z_k$ has monotonously decreasing amplitudes from the lowest possible frequency $\omega_{\min} \approx \gamma_{\min}^z/2\tau$ to the maximum one $\omega_{\max} \approx 4\gamma_{\min}^z/\tau$ (expressed in the limit of $N \to \infty$). This is also true for the case of interaction with the two frozen local impurities (e.g. for $J = \gamma$) as these have a minor effect on the electron Hamiltonian. For the parameters typically used in our simulations the corresponding maximum period $T_{\text{max}} = 2\pi/\omega_{\min}^z \lesssim 1$ ps is within the total time of the simulation while the corresponding minimum period $T_{\text{min}} = 2\pi/\omega_{\max}^z \approx 1$ fs is much larger than the typical time step $\Delta t = 0.01$ fs.

A more detailed spectral analysis is obtained by the two-dimensional dFT power portraits of $\Delta s^z_k$ (see Fig. 3) denoted as $\text{dFT}[\Delta s^z_k(t)](k,\omega)$. In Fig. 3 we compare such spectra for the itinerant spin-dynamics to its exact counterpart in the case of a finite homogeneous tight-binding chain. These portraits reveal key features of the one-dimensional fermionic system that vary systematically with the band-filling $\rho_0$, namely (i) a near-continuum of allowed modes in a certain $(k,\omega)$-space region, defined by a low- and a high-energy dispersion functions, (ii) a linear dispersion for small $k$ ($\omega \propto k$ for $k \to 0$). An analogous mode-occupation patterns have been rigorously analyzed in relation to the dynamical properties of one-dimensional quantum Heisenberg spin chains which too have a tight-binding type dispersion re-
The low-energy mode-occupation limit is due to the fact that the energy of the electron-hole excitation can approach zero only for $\Delta k \to 0$ and $\Delta k \to 2k_F$, where $k_F$ is the Fermi vector ($k_F = \frac{\pi}{a}$ for $\rho_0 = 0.5$, corresponding to one electron per site). The variation of the band filling away from the half-filling results into a folding of the low-energy limit as shown in Figs. 3(b), 3(c), 3(e) and 3(f). Note that due to electron-hole symmetry we only show the spectra for $\rho_0 \geq 0.5$.

![FIG. 3](image-url)

FIG. 3: (Color online) dFT $[\Delta s^z_i(t)](k, \omega)$ for different band-filling: (a, d) $\rho_0 = 0.5$ , (b, e) $\rho_0 = 0.6$ and (c, f) $\rho_0 = 0.8$. The top panels show the exact analytical excitation spectrum for a homogeneous tight-binding chain without local spins. The bottom panels show the results of our numerical simulations. The inter-site distance $a$ is arbitrary. The color shade in the bottom panel represents the absolute value of dFT $[\Delta s^z_i(t)](k, \omega)$ and is logarithmically scaled for better contrast.

B. Electrostatic gate applied

The dynamics of the itinerant spins, as described by Eq. (5), in the case of an electrostatic gate applied to a section of the wire (typically in the middle of the wire) cannot be expressed in a closed form as a function of $V_g$ for arbitrarily big systems. As such we resort to the two-dimensional dFT images (Fig. 5) of the spin dynamics in the presence of the gate bring additional dimension to the electron spectroscopy analysis. The difference here with respect to the case depicted in Fig. 3(d) is that a gate has been applied to the middle of the chain in the ground state, i.e. $V_g \sum_{|i, j|} c_{i}^{\dagger} c_{j}$ has been added to $H_{el}$ at $t = 0$. Again we use the half-filling case, $\rho_0 = 0.5$ (one electron per atom). From the figure it is nearly linearly with increasing $V_g$ (these are shown as red squares in Fig. 4). The spatial distribution of these eigenstates is predominantly concentrated in the gated region, i.e. they corresponds to the region where the local onsite energy has been modified.

![FIG. 4](image-url)

FIG. 4: (Color online) Schematic of the gate-dependence of the ground state energy spectrum of $H_{el}$. According to their weights at the three subsections of the chain $\Omega_{el, M, R} = \sum_{i \in \Omega_{el, M, R}} |\psi_i|^2$ we distinguish three types of states depending on which of the three partial weights is the greatest. We use black circles for the case of $\Omega_{el}$, red squares for $\Omega_{M}$ and green diamonds for $\Omega_{R}$. Note that the eigenstates corresponding to the two ungated regions ($\Omega_{el}$ and $\Omega_{R}$) are degenerate by symmetry, as the gate is applied in the exact center of the wire. The inset shows a magnification of an area of intermediate $V_g$, illustrating the situation of avoided crossings. A short chain with $N = 30$ sites is used for simplicity.

For extremely large values of $V_g$ ($V_g > 4\gamma$) the chain is effectively split into three energetically-decoupled parts, the gated middle and the two identical un-biased ends on the left-hand side and on the right-hand side. More interesting for us is the range of intermediate gate voltages, for which the three parts of the wire are substantially affected but not yet decoupled by the gate voltage. For such $V_g$ avoided crossings occur between states localized in the gated and non-gated regions. This gives rise to additional low-frequency lines in the dynamical spectrum as described by Eq. (5). As we will demonstrate in the Appendix the presence of these avoided crossings around the Fermi level for certain intermediate $V_g$ yields an enhanced transmission through the gated wire (waveguide) at low frequencies.

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immediately noticeable that the effect of the variation of $V_g$ on the excitation spectra is quite similar to the effect of the band-filling in the non-gated case. Due to the gate potential, the relative electron populations of the gated and gate-free parts of the chain change (the gated region is depopulated). For intermediate values of $V_g$ [see Fig. 5(b)] the excitation spectrum is rather a superposition of two spectra with band fillings below and above 0.5 (approximately 0.2 and 0.6). Furthermore we find a substantially increased population of the low-frequency modes for all $k$-vectors, i.e. of states were forbidden by symmetry for $V_g = 0$. For large $V_g$ [see Fig. 5(c)] the middle part of the wire becomes almost completely depleted and the $(k, \omega)$-portrait corresponds effectively to the excitation spectrum of a single chain with a bandfilling $\rho_0 \approx 0.75$, which is similar to the non-gated case presented in Fig. 3(f).

**FIG. 5:** (Color online) $\Delta$FT-portrait of the probe spin $S_1^x(t)$ for different values of the gate potential: (a) $V_g = 0.2 \gamma$, (b) $V_g = 2.2 \gamma$ and (c) $V_g = 4.6 \gamma$. The color shade is identical to that on Fig. 3.

**IV. COMBINED QUANTUM-CLASSICAL SPIN DYNAMICS IN THE PRESENCE OF A GATE**

The inclusion of dynamic local spin-impurities in the model requires the numerical integration of the set of coupled non-linear EOMs of Eq. [6]. For a small number of classical spins the dynamics of the itinerant spin-density is qualitatively very similar to what is described by Eq. [5]. The frequency-domain analysis of the classical spin trajectories by means of $\Delta$FT reveals the characteristic signature of the discrete electronic spectrum with only additional modulations in the amplitudes. We focus now on the case in which $S_1^x$ is driven by a local magnetic field into a precession, hence it acts as a spin-pump (see cartoon in Fig. 7). It is important to note that what we refer to as a local magnetic field $B = (0, 0, B^z)$ is only instrumental to trigger and sustain a uniform Larmor precession of $S_1$, i.e. it does not produce any Zeeman splitting in the itinerant electrons spectrum. We consider now the following situation: the quantum-classical spin-system is in its ground state until $t = t_0$, when the first local spin $S_1$ starts fluctuating to form a small misalignment with $B$. This sets the entire quantum-classical spin system into motion. The typical trajectories of the transverse components $S_1^y(t)$ and $S_1^z(t)$ and their frequency-domain $\Delta$FT images for different values of the gate voltage are presented in Fig. 6.

**FIG. 6:** (Color online) Time evolution of the $x$-components of the localized spins, $S_1^x(t)$ (blue) and $S_2^x(t)$ (red) [left] and the corresponding spectra, $\Delta$FT[$S_1^x(t)$]($\omega$), [right] for three different gate voltages (a, d) $V_g = 0.1 \gamma$, (b, e) $V_g = 2.2 \gamma$ and (c, f) $V_g = 4.6 \gamma$. The frequency-domain is represented by the dimensionless quantity $\tilde{\omega} = \omega / \gamma$ and $\tilde{\omega}_2 = \omega_2 / \gamma = 1.16$ for $\gamma = 1$ eV. Note that in the case of $V_g = 2.2 \gamma$ different scales are used for the magnitudes of $S_1^x(t)$ and $S_2^x(t)$ and their spectra (axes corresponding to $S_2^x(t)$ are marked in red).

In this case the excitation of a transverse spin-density at $t = 0$ by the initiation of the Larmor precession is very similar in nature to the excitation induced by tilting one local spin investigated before (section III). In fact it indeed develops in a very similar way in the early stages of the time evolution. Just like in Fig. 2 a non-equilibrium transverse spin-density spin packet is sent along the wire and both the localized spins respond each time the packet reaches them. Figure 6(a) displays the case of a very small gate voltage $V_g \ll \gamma$. The frequency-domain image of the precessional motion of $S_1^x(t)$ has the signature of the discrete electronic spectrum with an amplitude envelope that peaks at the Larmor frequency $\omega_1 = 2 \mu_B B_1 / h$. The $\Delta$FT-portrait of the probe spin $S_2^x(t)$ is very similar to that of $S_1^x(t)$. Although significantly down-scaled in amplitude, it has the electronic-structure modes imprinted in its classical motion in the same way as it is for the driven spin. This qualitative behavior is observed for $V_g = 0$ and a range of small voltages $V_g \lesssim \gamma$ but it changes dramatically for gate voltages $V_g \gg \gamma$ [see Fig. 6(b) and (c)]. The case of extremely big voltages $V_g > 4 \gamma$ (depicted in the bottom panel) is a trivial one for which the electrostatic barrier $V_g$ is completely opaque to the electrons and the probe spin $S_2$ does not respond to the Larmor precession of $S_1$ (note also the rarefaction of modes in the $S_1^x$ spectrum due to the effective shortening of the chain by $2/3$).

Special attention must be devoted to the intermediate
In the $V_g$ regime in which the dynamics of the probe spin is qualitatively different and uncorrelated to that of the driven one [see Fig. 6(b)]. The typical outcome of the real time dynamics at such intermediate voltages $\gamma < V_g < 4\gamma$ is that the probe spin starts accumulating very big transverse deflections. This is then fed back into the pumping spin which also deflects more but still preserves, to a great extent, its precession about the magnetic field.

It is worth noting that this self-amplification of the spin-dynamics does not come at a total energy cost, as the model system described by Eq. (2) is completely conservative. As such we simply observe a conversion of electrostatic energy into "spin-energy" in the form of a spin amplitude transverse to the driving magnetic field. This accumulation is related to the increasing energy transfer from the itinerant electrons to the localized spins. While around $\omega_0$, the shape of the spectrum of $S_1$ is similar to the two extreme $V_g$ cases, a significant amplitude is accumulated now at low frequencies. The main difference from the small $V_g$ case, however, is in the spectrum of $S_2$ which shows practically no response at the Larmor frequency but has very large amplitudes in the low frequency range.

This behaviour in the classical spin dynamics characteristic of certain gate voltages stems from the dominance of the low frequency modes in the electron dynamics at those $V_g$. The effect can be seen also in the much simpler case of a non-spin-polarized uniform atomic wire subjected to a sudden switch of an electrostatic gate in the middle. In the Appendix we consider the charge dynamics associated to this situation and analyze the lowest frequency components entering in Eq. (5). The initial charge excitation, similarly to the transverse spin polarization in the model above, is triggered by a local electrostatic perturbation at the first site. It follows from Eq. (5) that, for certain values of $V_g$ for which two adjacent adiabatic eigenenergies $(e_i, e_{i+1})$ around the Fermi level come closer to each other in an avoided crossing, the dynamical charge amplitude at the opposite end of the wire exhibits a peak at that particular very low frequency $(e_{i+1} - e_i)/\hbar$. In other words, a certain gate voltage condition is created for resonant charge transfer between the three parts of the chain at low frequencies. This, in the case of itinerant transverse spin-polarization, promotes the enhanced reaction of the probe spin to the spin pumping produced on the other side of the gate.

The electronic part of full quantum-classical spin dynamics in the presence of the gate (Fig. 6) is, in many respects, similar to the charge-only case, described in Section IV and in the Appendix. As before we construct the two-dimensional dFT portraits of the spin-density evolution. Providing additional $k$-resolved information these give another perspective for interpreting the dramatic increase of the low-frequency oscillations of the probe spin at certain gate voltages, when compared to the case of frozen $S_i$ and electrons at $t = t_0 - \delta t$ relaxed to the external gate potential (Fig. 5). In the latter case, the increased low-frequency occupations (with respect to the non-gated case) were attributed to the split of the one-dimensional system into subsystems with different average electron densities. Here we find a similar dFT pattern, now in the presence of dynamically-coupled local spins and a gate abruptly introduced at $t = t_0$. Those two additional time-dependent factors result in a significant variation in time of the electron distributions in the gated and non-gated segments of the chain [see Fig. 7(b)]. The dFT image in this case can be interpreted as a superposition of spectra corresponding to different $\rho_0$, resulting in a smearing of the low-frequency structure previously present in the $(k, \omega)$-space image. A comparison of the results for $V_g = 0$ and $V_g = 2.2\gamma$ is presented in Fig. 5. We find that the full dynamical $V_g = 0$ portrait is rather similar to the results obtained for frozen-impurities (see Fig. 5), the only additional feature being the adiabatic excitation at the Larmor frequency of the driven spin. The difference (point-by-point subtraction of the contour plots) with the corresponding gated case, depicted Fig. 8(b) shows that it is indeed mainly the lower frequency band of the spectrum (for any wave-vector)
that gains occupation in the gated case.

\[ d_{\text{FT}}[\Delta(t)](k,\omega) \text{ for } V_g = 0. \]
\[ d_{\text{FT}}[\Delta(t)](k,\omega) \text{ for } V_g = 2.2\gamma \text{ and for } V_g = 0 \text{ defined as } \Delta = |d_{\text{FT}}[\Delta(t)](k,\omega)|_{V_g=2.2\gamma} - d_{\text{FT}}[\Delta(t)](k,\omega)|_{V_g=0}. \]

The color shade represents the absolute value of \( d_{\text{FT}}[\Delta(t)](k,\omega) \) and \( \Delta \), respectively, and is logarithmically scaled for better contrast.

\[ \text{FIG. 8: (a) } d_{\text{FT}}[\Delta(t)](k,\omega) \text{ for } V_g = 0. \text{ (b) The difference between } d_{\text{FT}}[\Delta(t)](k,\omega) \text{ for } V_g = 2.2\gamma \text{ and for } V_g = 0. \]

V. CONCLUSIONS

In summary, we have employed atomistic dynamical simulations to investigate the effect of an electrostatic gate as means of controlling the indirect coupling between two distant localized spin impurities in a finite metallic wire comprising one hundred atoms. One of the impurities, precessing in external magnetic field, plays the role of a spin-pump and the response of the second (probe) spin was analyzed as a function of the gate potential applied to the interconnecting wire. We identified a range of external gate potentials for which the spin-pumping is extremely efficient and leads to a substantial excitation of transversely-polarized itinerant spin density in the non-gated parts of the chain. This, in turn, produces a massive low-frequency swing of the probe spin. Such a resonant effect has been related to gate-induced avoided crossings in the electronic structure of the interconnect. For certain gate voltages these occur in the vicinity of the Fermi level and assist the enhanced transfer of charge/spin across the barrier. Evidences for this effect are also identified in the Fourier portraits of the calculated time-dependent spin-distribution.

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Appendix

We consider the eigenstate-resolved dynamical amplitude \( A_{mn} \) corresponding to a mode with frequency \( \omega_{mn} \), associated to the transitions between the eigenstates \( e_m \) and \( e_n \). The system is the simplified wire used for the spectroscopic analysis of Fig. 4 i.e. it is a non-spin-polarized 30-atom long chain. Analogously to the spin-polarized case, the \( t = t_0 \) excitation is applied simply as a potential shift at the first atomic site. From Eq. (5) the dynamically-driven charge-accumulation amplitude at site \( i \) is defined as

\[ A^i_{mn} = c_m c^*_n \sum_{kl} c_{kn} c_{in} \rho_{kl}(t_0), \]  

such that

\[
\rho_{ii}(t) = \sum_{mn} A^i_{mn} e^{-i\omega_{mn}t} \]  

is the dynamic electron occupation at site \( i \). This quantity is calculated at the last site, \( i = N \), i.e. at the opposite side of the chain with respect to the perturbation. In Eq. (A.1) \( c_{im} = \langle i|\varphi_m \rangle \) are the onsite components of the eigenvectors \( |\varphi_m \rangle \) of the non-spin-polarized Hamiltonian \( H_{el}(V_g) \) for which the gate voltage \( V_g \) is applied (between the sites \( i = 11 \) and \( i = 21 \)).

From all the pairs of adjacent eigenstates \( (\epsilon_i, \epsilon_{i+1}) \), which have the highest (in absolute value) amplitude \( A^N_{i,i+1} \). For small gate voltages these are the eigenstates around the Fermi level but as \( V_g \) increases the modes with the largest amplitudes tend to arise where avoided crossings of eigenstates occur. These are also the modes with frequencies close to the lowest possible frequency for that particular gate voltage.

The actual highest amplitude at the last site, corresponding to the highlighted modes in Fig. 9 are depicted as a function of \( V_g \) in Fig. 10(a), together with the quantity \( A^N_{i,i+1} = \sqrt{\sum (A^N_{i,i+1})^2} \). This represents the pessimistic estimate (considering all modes orthogonal in phase) of the total low-frequency amplitude corresponding to all pairs of adjacent eigenvalues. Such curves demonstrate the resonant nature of the dynamical site-occupation as a function of the gate voltage. Fig. 10(a) also shows that the low frequency charge excitation peaks for intermediate gate voltages (for this case \( V_g \sim 2.5\gamma \)) can be related to the observed enhanced low-frequency coupling between the itinerant and localized spins for the intermediate \( V_g \) range. Interestingly, the two \( A(V_g) \) curves coincide for very low and very high voltages, showing that in this case the entire dynamics is practically due to just one mode (marked in black in Fig. 9). In the intermediate regime it is clear that there are more than one low-frequency modes which have a significant amplitude, although the one marked in Fig. 9 gives the leading contribution.
FIG. 9: (Color online) Adiabatic variation with the gate voltage of a few eigenvalues around the Fermi level (we have used $\varepsilon_0 = 0$ and $|\gamma| = 1$ eV, hence $E_F = 0$ at $V_g = 0$). Marked with black lines are the pairs of eigenstates $(i, i+1)$ which give rise to the highest (in absolute value) dynamical amplitude $A_{N,i,i+1}$ at the last site $N$.

FIG. 10: (Color online) (a) The maximum single-mode amplitude $A_{N_{\text{max}}}$ and an estimate for the total low-frequency amplitude $A_{N_{\text{sum}}}^N$ (see text for details) as a function of the applied gate voltage. (b) The frequency of the mode related to the pair of eigenstates $(i = 15)$ around the Fermi level, adiabatically evolved with the gate voltage and (c) its corresponding amplitude as defined in Eq. (A.1).

For a particular pair of adjacent eigenstates there are a few instances where the adiabatic eigenvalues come closer together as a function of the gate voltage. In Fig. 10(b,c) we analyze the dependence of the frequency and the amplitude corresponding to the pair of eigenvalues just below and above the Fermi level in the ground state ($i = 15$ for the 30-atom chain at half-filling). We find that the dynamical charge amplitude on the last site peaks (as absolute value) every time the frequency passes through a minimum.

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This region can also be re-interpreted as part of a different material so that the same model system also describes a one-dimensional tri-layered heterostructure in which the two peripheral layers are identical.

This effect can appear as a particular form of “heating” for the local spins, at the expense of electron gas, as within the time covered by the simulation (≈10 ps) the energy transfer seems to be irreversible. It is well-known, however, that the typical Ehrenfest molecular dynamics (EMD) suffers from the inability to account for Joule heating processes due to the lack of dynamical correlations between the electrons and the ions. Our simulations are limited to picosecond times and by no means imply a possible qualitative difference of the EMD and its spin counterpart.