Water loss from terrestrial planets orbiting ultracool dwarfs: implications for the planets of TRAPPIST-1

E. Bolmont, ⋆ F. Selsis, 2, 3 ⋆ J. E. Owen, 4 ⋆ I. Ribas, 5 S. N. Raymond, 2, 3 J. Leconte 2, 3 ⋆ and M. Gillon 6

1 NaXys, Department of Mathematics, University of Namur, 8 Rempart de la Vierge, B-5000 Namur, Belgium
2 Univ. Bordeaux, LAB, UMR 5804, F-33615 Pessac, France
3 CNRS, LAB, UMR 5804, F-33615 Pessac, France
4 Institute for Advanced Study, Einstein Drive, Princeton, NJ 08540, USA
5 Institut de Ciències de l’Espai (CSIC-IEEC), Carrer de Can Magrans s/n, Campus UAB, E-08193 Bellaterra, Spain
6 Institut d’Astrophysique et de Géophysique, Université de Liège, Allée du 6 Août 19C, B-4000 Liège, Belgium

Accepted 2016 October 6. Received 2016 October 5; in original form 2016 May 2; Editorial Decision 2016 October 5

ABSTRACT

Ultracool dwarfs (UCD; T eff < ∼ 3000 K) cool to settle on the main sequence after ∼ 1 Gyr. For brown dwarfs, this cooling never stops. Their habitable zones (HZ) thus sweeps inward at least during the first Gyr of their lives. Assuming they possess water, planets found in the HZ of UCDs have experienced a runaway greenhouse phase too hot for liquid water prior to enter the HZ. It has been proposed that such planets are desiccated by this hot early phase and enter the HZ as dry worlds. Here, we model the water loss during this pre-HZ hot phase taking into account recent upper limits on the XUV emission of UCDs and using 1D radiation-hydrodynamic simulations. We address the whole range of UCDs but also focus on the planets recently found around the 0.08 M ⊙ dwarf TRAPPIST-1. Despite assumptions maximizing the FUV photolysis of water and the XUV-driven escape of hydrogen, we find that planets can retain significant amount of water in the HZ of UCDs, with a sweet spot in the 0.04–0.06 M ⊙ range. We also studied the TRAPPIST-1 system using observed constraints on the XUV flux. We find that TRAPPIST-1b and c may have lost as much as 15 Earth oceans and planet d – which might be inside the HZ – may have lost less than 1 Earth ocean. Depending on their initial water contents, they could have enough water to remain habitable. TRAPPIST-1 planets are key targets for atmospheric characterization and could provide strong constraints on the water erosion around UCDs.

Key words: planets and satellites: atmospheres – planets and satellites: individual: TRAPPIST-1 – planet star interactions – brown dwarfs – stars: low-mass.

1 INTRODUCTION

Earth-like planets have been detected in the habitable zones (HZs; defined in Kasting, Whitmire & Reynolds 1993; Selsis et al. 2007b; Kopparapu et al. 2013) of early-type M-dwarfs (e.g. Quintana et al. 2014). Here, we address the potential habitability of planets orbiting even less-massive objects: ultracool dwarfs (UCDs), which encompass brown dwarfs (BDs) and late-type M-dwarfs. The first gas giant was detected around a BD by Han et al. (2013). Very recently, Gillon et al. (2016) discovered three Earth-sized planets close to an object of mass 0.08 M ⊙ (just above the theoretical limit of $M_e \sim 0.075 M_\oplus$) between BDs and M-dwarfs, Chabrier & Baraffe (1997). The two inner planets in this system have insolations between 4.25 and 2.26 times the insolation of the Earth. The orbital period of planet d is still undetermined but between 4.5 and 73 d. The planet receives a stellar flux in the range 0.02–1 times the stellar flux of Earth, which includes a large fraction of the HZ of Trappist-1 (0.023–0.048 au, Kopparapu et al. 2013). The atmospheres of these planets could be probed with facilities such as the Hubble Space Telescope (HST) and James Webb Space Telescope (JWST), which makes them all the more interesting to study (Barstow & Irwin 2016).

BDs (i.e. objects of mass 0.01 ≤ $M_\ast/M_\odot$ ≤ 0.07) do not fuse hydrogen in their cores (Spiegel, Burrows & Milsom 2011). They contract and become fainter in time. Their HZs therefore move inward in concert with their decreasing luminosities (Andreasen & Scal 2004; Bolmont, Raymond & Leconte 2011). Nonetheless, for BDs more massive than a 0.04 M ⊙ planet on a fixed or slowly

* E-mail: emeline.bolmont@unamur.be (EB); franck.selsis@u-bordeaux.fr (FS); jeremy.leconte@u-bordeaux.fr (JL)
† Hubble Fellow.
evolving orbit can stay in the HZ for Gyr time-scales (Bolmont et al. 2011). In this study, we consider UCDs of mass up to 0.08 M\(_{\odot}\). A UCD of mass 0.08 M\(_{\odot}\) is actually a late-type M-dwarf. As for a BD, its luminosity also decreases with time but its mass is high enough so that it starts the fusion of hydrogen in its core. From that moment, the HZ stops shrinking, allowing close-in planets to stay more than 10 Gyr in the HZ. However, any planet that enters the HZ has spent time in a region that is too hot for liquid water. A planet experiencing a runaway greenhouse around a Sun-like star is expected to lose considerable amount of water (one Earth ocean in less than one Gyr). This is due to H\(_2\)O photolysis by FUV photons and thermal escape of hydrogen due to XUV heating of the upper atmosphere. The current scenario to explain the water depletion in the atmosphere of Venus and its high enrichment in deuterium (Solomon et al. 1991). Could planets in the HZs of UCDs, such as Venus, have lost all of their water during this early hot phase?

Barnes & Heller (2013) found that planets entering the BD HZ are completely dried out by the hot early phase. They concluded that BDs are unlikely candidates for habitable planets. Here, we present a study of water loss using more recent estimates for the X-ray luminosity of very low-mass stars and confronting results obtained with 1D radiation-hydrodynamic mass-loss simulations. We find that – even in a standard case scenario for water retention – a significant fraction of an initial water reservoir (equivalent to one Earth ocean, M\(_{\text{H,O}}\) = 1.3 \times 10^{21} \text{ kg}) could still be present upon reaching the HZ. Once planets enter the HZ, the water can condense on to the surface (as is thought happened on the Earth, once the accretion phase was over; e.g. Matsui & Abe 1986; Zahnle, Kasting & Pollack 1988). Observation of these objects, such as the TRAPPIST-1 planets, would probably lift this uncertainty.

2 ORBITAL EVOLUTION OF PLANETS IN THE ULTRACOOL DWARF HABITABLE ZONE

The UCD HZ is located very close-in, at just a few per cent of an astronomical unit (or less; Bolmont et al. 2011). Tidal evolution is therefore important. Due to UCDs’ atmospheres low degree of ionization (Mohanty et al. 2002) and high densities, magnetic breaking is inefficient and cannot counteract spin-up due to contraction. UCDs’ corotation radii – where the mean motion matches the UCD spin rate – move inward.

Fig. 1 shows the evolution of the HZ boundaries for two UCDs: one of mass 0.01 M\(_{\odot}\) and other of mass 0.08 M\(_{\odot}\). The time at which a planet reaches the HZ depends on its tidal orbital evolution as well as the cooling rate of the UCD. The tidal evolution of a planet around a UCD is mainly controlled by its initial semimajor axis with respect to the corotation radius (in red and orange full lines in Fig. 1). A planet initially interior to the corotation radius migrates inwards due to the tide raised in the UCD and eventually falls on the UCD. A planet initially outside corotation migrates outward (Bolmont et al. 2011). There does exist a narrow region in which the moving corotation radius catches up to inward-migrating planets and reverses the direction of migration. The planet’s probability of survival is smaller the farther inwards it is from the corotation radius, which is illustrated by the coloured gradient area in Fig. 1.

Surviving planets cross the shrinking HZ at different times depending on their orbital distance. Close-in planets tend to stay longer in the HZ because the UCDs’ luminosity evolution slows as it cools (Chabrier & Baraffe 1997). Bolmont et al. (2011) showed that for UCDs of mass higher than 0.04 M\(_{\odot}\), planets can spend up to several Gyr in the HZ. Although their earlier tidal histories vary, planets are completely dried out by the hot early phase. They concluded that BDs are unlikely candidates for habitable planets. Here, we present a study of water loss using more recent estimates for the X-ray luminosity of very low-mass stars and confronting results obtained with 1D radiation-hydrodynamic mass-loss simulations. We find that – even in a standard case scenario for water retention – a significant fraction of an initial water reservoir (equivalent to one Earth ocean, M\(_{\text{H,O}}\) = 1.3 \times 10^{21} \text{ kg}) could still be present upon reaching the HZ. Once planets enter the HZ, the water can condense on to the surface (as is thought happened on the Earth, once the accretion phase was over; e.g. Matsui & Abe 1986; Zahnle, Kasting & Pollack 1988). Observation of these objects, such as the TRAPPIST-1 planets, would probably lift this uncertainty.

3 MODELING WATER LOSS

3.1 Energy-limited escape formalism

In order to place the strongest possible constraints, we calculate the mass-loss of the atmosphere via energy-limited escape (Watson, Donahue & Walker 1981; Lammer et al. 2003). During a runaway phase, water is able to reach the stratosphere without condensing. Assuming photolysis is not a limiting process, water is photodissociated. In order to escape, water needs to reach the base of the hydrodynamic wind, which is much higher up. We here make the hypothesis that this is the case. In this work, we do not consider the diffusion-limited escape, which would be responsible for a lower escape rate than the energy-limited escape rate. The presence of other gases not considered here could bottleneck the diffusion of water vapour into the upper atmosphere. The energy-limited

\[1 \text{ In the worst case, i.e. if the UCD is very dissipative, this would mean that we underestimate the mass-loss by } \sim 1 \text{ per cent.} \]
escape mechanism requires two types of spectral radiation: FUV (100–200 nm) to photodissociate water molecules and XUV (0.1–100 nm) to heat up the exosphere. This heating causes atmospheric escape when the thermal velocity of atoms exceeds the escape velocity above the exobase. Non-thermal loss induced by stellar winds can in theory contribute significantly to the total atmospheric loss, either by the quiescent wind or by the coronal ejections associated with flares (Lammer et al. 2007; Khodachenko et al. 2007). For earlier type UCDs, this might be an issue, however we here consider UCDs of spectral type later than M7 type, for which there is no indication of winds that could enhance the atmospheric loss (due to the low degree of ionization, see Mohanty et al. 2002).

Energy-limited escape considers that the energy of incident radiation with $\lambda < 100 \text{ nm}$ is converted into the gravitational energy of the lost atoms. This formalism was used in many studies (e.g. Barnes & Heller 2013; Heller & Barnes 2015; Luger & Barnes 2015) but we use here the prescription of Selsis et al. (2007a) linking the XUV flux $\dot{F}_{\text{XUV}}(\text{at } d = 1 \text{ au})$ to the mass-loss rate $\dot{m}$:

$$\frac{\dot{F}_{\text{XUV}} \pi R_p^2}{(a / 1 \text{ au})^2} = \frac{G M_p m}{R_p},$$

where $R_p$ is the planet’s radius, $M_p$ its mass and $a$ its semimajor axis. $\epsilon$ is the fraction of the incoming energy that is transferred into gravitational energy through the mass-loss. This efficiency is not to be confused with the heating efficiency, which is the fraction of the incoming energy that is deposited in the form of heat, as only a fraction of the heat drives the hydrodynamic outflow (some being for instance conducted downward). This fraction has been estimated at about 0.1 by Yelle (2004) and more recently at 0.1 or less in the limit of extreme loss by Owen & Wu (2013). The left term of equation (1), $F_{\text{XUV}} \pi R_p^2 / (a / 1 \text{ au})^2$, corresponds to the fraction of the XUV flux intercepted by the planet. Thus, the mass-loss rate is given by

$$\dot{m} = \epsilon \frac{F_{\text{XUV}} \pi R_p^3}{G M_p (a / 1 \text{ au})^2}.$$

(2)

Taking into account that the planet might undergo orbital migration or the evolution of the XUV flux the mass lost by the planet at a time $t$ is of

$$\dot{m} = \epsilon \frac{\pi R_p^3}{G M_p} \int_0^t F_{\text{XUV}} (a / 1 \text{ au})^2 \, dt.$$

(3)

One could argue that the XUV cross-section radius of the planet is larger than the planet’s radius and is probably similar to the Hill radius (as in Erkaev et al. 2007, which considered Jupiter-mass planets). This assumption would mean that the mass-loss would be higher than what we propose to calculate here. In a hydrodynamic outflow the effect of the Roche lobe is to weaken the effect of gravity compared to the pressure force, its role is felt through the gradient of the potential. For transonic outflow the distance of the sonic point from the surface of the planet depends on the gradient of the potential, with shallow gradients (i.e. closer to the Hill radius) pushing the sonic point closer to the planet increases the mass-loss. We tested our hypothesis of taking the real radius of the planet with a hydrodynamical code (see Section 3.3 and Owen & Alvarez 2016). We find that, for the small rocky planets we consider here, this does not underestimate the mass-loss as much as the work of Erkaev et al. (2007) would imply (taking the Roche radius), as the effect is of the order of a few per cent.

Venus probably lost its water reservoir by this mechanism. Radar observations of the Magellan satellite and ground-based observations showed that the last traces of water on Venus date back at least 1 billion years (this corresponds to the age of the surface; Solomon et al. 1991). Venus certainly experienced energy-limited hydrodynamic loss of water during several billion years (Chassefière et al. 2012). As UCDs are less bright than the Sun, we expect their XUV flux to be lower than the XUV flux of Sun.

In order to calculate the mass-loss, we therefore need the XUV flux of the dwarfs and estimate the efficiency $\epsilon$. In the following, we give the observational constraints on the XUV luminosity of UCDs of spectral type later than M7 type. We then use these values to compute the efficiency $\epsilon$ using 1D radiation-hydrodynamic mass-loss simulations.

### 3.2 Physical inputs

We first assume that protoplanetary discs around UCDs dissipate after 3 Myr (Pascucci et al. 2009; Pecaut & Mamajek 2016); it is our ‘time zero’. This is a strong assumption, it is possible that discs live much longer than that, ~10 Myr according to Pfalzner, Steinhausen & Menten (2014). We consider that when the planet is embedded in the disc, it is protected and does not experience mass-loss.

Plants are thought to acquire water during and after accretion via impacts of volatile-rich objects condensed at larger orbital radii. On the one hand, if planets form in situ in the HZs of UCDs then it may be difficult to retain water because of the rapid formation of time-scale and very high impact speeds (Lissauer 2007; Raymond, Scalo & Meadows 2007). On the other hand, because they form fast while embedded in a disc, they can acquire volatiles directly from the disc itself. It has been suggested that accreting H$_2$ this way can lead to the formation of H$_2$O (Ikoma & Genda 2006). In contrast, if these planets or some of their constituent planetary embryos migrated inward from wider orbital distances then they are likely to have significant water contents (Raymond, Barnes & Mandell 2008; Ogihara & Ida 2009). Although the origin of hot super-Earths is debated (see Raymond et al. 2008; Raymond & Cossou 2014), several known close-in planets are consistent with having large volatile reservoirs (e.g. GJ 1214 b; Rogers & Seager 2010; Berta et al. 2012). We therefore consider it plausible for Earth-like planets to form in the UCD HZ with a water content at least comparable to Earth’s surface reservoir and possibly much bigger. For example, the Earth contains several additional oceans of water trapped in the mantle (Marty 2012). Water can also be trapped in the mantle of a planet during the formation process and perhaps released later in the atmosphere through volcanic activity.

A key input into our model is the stellar flux at high energies. There are no observations of the EUV flux of UCDs. We assume here that the loss rate of water is not limited by the photodissociation of water. This assumes that FUV radiation is sufficient to dissociate all water molecules and produce hydrogen at a rate higher than its escape rate into space. X-ray observations with Chandra/ACIS-I2 exist for objects from M6.5 to L5 (e.g. Berger et al. 2010; Williams, Cook & Berger 2014) for the range 0.1–10 keV (0.1–12.4 nm). This only represents a small portion of the XUV range considered in equations (2) and (3). For solar-type stars, the flux in the whole XUV range is two to five times higher than in the X-ray range (Ribas et al. 2005). We thus multiply the value corresponding to the X-ray range by 5. This constitute an upper limit of what one might expect, indeed for active UCDs the factor can be lower than 2 (e.g. for TRAPPIST-1 this factor is of 1.78, Wheatley et al. 2016). We consider here that it can be used as a proxy for the whole XUV range.
On one hand, observations of objects of spectral types M0–M7 show that the X-ray luminosity scales as $10^{-3}$ the bolometric luminosity $L_{\text{bol}}$ (Pizzolato et al. 2003). On the other hand, more recent observations from Berger et al. (2010) and Williams et al. (2014) show that the X-ray luminosity of L dwarfs seems to scale as $10^{-5} \times L_{\text{bol}}$. However, some of these observations are actually non-detections, so the X-ray luminosity of objects such as 2M0523–14 (L2–L3), 2M0036+18 (L3–L4) and 2M1507–16 (L5) must be even lower than $10^{-5} \times L_{\text{bol}}$. Between the populations of dwarfs of spectral types M0–M7 and those of spectral types L0–L6, there are dwarfs of spectral types M8 and M9 that do not really follow either trends. TRAPPIST-1 belongs to this transition population. That is why to study the water loss for the TRAPPIST planets, we considered a wide range of XUV-luminosities that are representative of this transition region: from $L_X/L_{\text{bol}} < 10^{-5}$ (as the analogue dwarf VB 10 (Williams et al. 2014)) to $L_X/L_{\text{bol}} < 10^{-3.4}$ (recent observations from Wheatley et al. 2016). There is no indication of whether the X-ray luminosity varies in time.

For the UCDS of mass 0.01 $M_\odot/M_\odot < 0.08$, we consider two limiting cases for our mass-loss calculation. In the first we adopt a value of $10^{-5} \times L_{\text{bol}}$. As the bolometric luminosity changes with time, we consider that the X-ray luminosity does as well. In the second case, we assume that the X-ray luminosity does not vary with the bolometric luminosity but rather remains constant. We adopt the value of $10^{25.4} \text{ erg s}^{-1} = 2.5 \times 10^{18} \text{ W}$ from Williams et al. (2014). This value corresponds to a X-ray detection (0.1–10 keV) of the object 2M2541059 AB of spectral type L2. To take into account the fact that the dwarfs with the higher masses considered in the range 0.01 $M_\odot/M_\odot < 0.08$ are possibly part of the transition population, we also tested two additional cases corresponding to a higher XUV emission: $L_X/L_{\text{bol}} < 10^{-4.5}$ and $L_X = 10^{26} \text{ erg s}^{-1}$. For each case we then use equation (3) to calculate the mass-loss of a planet of 0.1, 1 and 5 $M_\odot$.

We compared the XUV flux received by the planets of Fig. 1 to the one Earth receives. Before reaching the HZ, they are at least a few times higher than Earth’s incoming XUV flux.

### 3.3 Estimation of $\epsilon$ with a hydrodynamical code

In order to guide our calculations, we perform a set of 1D radiation-hydrodynamical mass-loss simulations based on the calculations of Owen & Alvarez (2016). The simulations are similar in setup to those described by Owen & Alvarez (2016), where we perform 1D spherically symmetric simulations using a modified version of the ZEUS code (Stone & Norman 1992; Hayes et al. 2006), along a streamline connecting the star and planet. We include tidal gravity, but neglect the effects of the Coriolis force as it is small while the outflow remains sub-sonic (Murray-Clay et al. 2009; Owen & Jackson 2012). The radial grid is non-uniform and consists of 192 cells, the flow is evolved for 40 sound crossing times (see Owen & Alvarez 2016). The simulations are similar in setup to those described by Owen & Alvarez (2016), where we perform 1D spherically symmetric simulations using a modified version of the ZEUS code (Stone & Norman 1992; Hayes et al. 2006), along a streamline connecting the star and planet. We include tidal gravity, but neglect the effects of the Coriolis force as it is small while the outflow remains sub-sonic (Murray-Clay et al. 2009; Owen & Jackson 2012). The radial grid is non-uniform and consists of 192 cells, the flow is evolved for 40 sound crossing times such that a steady state is achieved (which is checked by making sure the pseudo-Bernoulli potential and mass flux are constant). We explicitly note that these simulations of a pure hydrogen atmosphere do not include line cooling from oxygen that maybe important in these flows, and as such these calculations should be considered as a maximum rate, as any other elements would lower the hydrogen loss by cooling the flow and colliding with the hydrogen atoms.

We can use the simulations to calculate the efficiency ($\epsilon$) parameter along with the corresponding mass-loss. Fig. 2 shows the variation of $\epsilon$ with the incoming XUV flux, we note that the tidal gravity places a negligible role in changing the mass-loss rates with stellar mass. At high fluxes, the efficiency drops off due to the increased radiative cooling that can occur as the flows get more vigorous and dense. The drop off at low fluxes is simply caused by the fact that the heating rate is not strong enough to launch a powerful wind. At high fluxes, the temperature peaks at a radius $\sim 1.2–1.4 R_\odot$, indicating some of the XUV photons are absorbed far from the planet, increasing its effective absorbing area, but at low fluxes the temperature peaks close to 1 $R_\odot$. Fig. 2 shows that for an X-ray luminosity of $L_X = 10^{25.4}$ erg s$^{-1}$ (corresponding to a flux in XUV of $\sim 450$ erg s$^{-1}$ cm$^{-2}$), assuming an efficiency $\epsilon$ of 0.1 as is typically the case in energy-limited escape calculations, overestimates the mass-loss by a factor of $\sim 1.17$.

Using these 1D radiation-hydrodynamic mass-loss simulations (see Owen & Alvarez 2016), we find that the temperature $T$ of the wind is of the order of 3000 K, which is much lower than calculated for hot Jupiters (of the order of $10^4$ K, e.g. Lammer et al. 2003; Erkaev et al. 2007; Murray-Clay et al. 2009).

### 3.4 The joint escape of hydrogen and oxygen

The computed mass-loss $\dot{m}$ is linked to a mass flux $F_M$ given by: $F_M = \dot{m}/(4\pi R_p^2)$. We consider here a mass-loss, but do not compute the proportion of hydrogen and oxygen atoms lost. Losing just hydrogen atoms and losing hydrogen and oxygen atoms do not have the same consequence for water loss. For example, if only hydrogen atoms are lost, losing an ocean means that the planet loses the mass of hydrogen contained in one Earth ocean (nine times lower that the mass of water in one Earth ocean). This would change the proportion of H/O thus preventing any later recombination of water (e.g. for Venus, Gillmann, Chassefière & Lognonné 2009). In contrast, if the planet loses hydrogen and oxygen in a stoichiometric proportion, losing an ocean means that the planet is losing the mass of water contained in one Earth Ocean. This is the more favourable case for water retention because it requires a higher energy to lose one ocean.

In the following, we estimate the proportion of escaping hydrogen and oxygen atoms. The mass-loss flux $\dot{m}_H F_M$ (kg $s^{-1}$ m$^{-2}$) can be expressed in terms of the particle fluxes (atoms $s^{-1}$ m$^{-2}$):

$$\dot{m}_H F_M = m_H F_H + m_O F_O.$$
The ratio of the escape fluxes of hydrogen and oxygen in such an hydrodynamic outflow can be calculated following Hunten, Pepin & Walker (1987):

\[ r_f = \frac{F_O}{F_H} = \frac{X_O m_O - m_O}{X_H m_H - m_H}, \]

where \( m_O \) is the mass of one oxygen atom, \( m_O \) is the mass of one hydrogen atom and \( m_{\epsilon} \) is called the cross-over mass and is defined by:

\[ m_{\epsilon} = m_H + \frac{kT F_H}{bg X_H}, \]

where \( T \) is the temperature in the exosphere, \( g \) is the gravity and \( b \) is a collision parameter between oxygen and hydrogen. In the oxygen and hydrogen mixture, we consider \( X_O = 1/3 \), \( X_H = 2/3 \), which corresponds to the proportion of dissociated water. This leads to \( X_O/X_H = 1/2 \).

When \( m_{\epsilon} < m_O \), only hydrogen atoms are escaping and \( F_H = F_M/m_H \). When \( m_{\epsilon} > m_O \), hydrogen atoms drag along some oxygen atoms and

\[ F_M = (m_H + m_O r_f) F_H. \]

With equations (5), (6) and (7), we can compute the mass flux of hydrogen atoms:

\[ F_H = \frac{F_M + m_O X_O (m_O - m_H) \frac{bg}{m_H + m_O X_H}}{m_H + m_O X_H}. \]

In order to calculate the flux of hydrogen atoms, we need an estimation of the XUV luminosity of the star considered, as well as an estimation of the temperature \( T \). We use the estimations of the XUV flux of Section 3.2 and the estimation of \( \epsilon \) and \( T \) obtained with the 1D radiation-hydrodynamic mass-loss simulations (Owen & Alvarez 2016).

We assume that the XUV luminosity here is \( L_0 = 5 \times L_X = 5 \times 10^{25.4} \text{ erg s}^{-1} \), that the planet is at \( a = 0.013 \text{ au} \) and following Section 3.3 (Fig. 2), we assume here \( \epsilon = 0.097 \). This is our baseline case. Using these values and equation (2), we can compute the mass-loss flux \( F_M = F_0 \) for a 1 M_\oplus planet:

\[ F_0 = \frac{m}{4\pi R_p^2} = \frac{F_{\text{XUV}} R_p}{4G M_p (a/1 \text{ au})^2} = 1.02 \times 10^{-10} \text{ kg s}^{-1} \text{ m}^{-2}. \]

Using equation (8) and the estimation of \( T \), we can compute the flux of hydrogen atoms \( F_H \) as a function of the XUV luminosity \( L_{\text{XUV}} \) compared to our baseline case luminosity \( L_0 \). Fig. 3 shows the behaviour of the mass-loss of the atmosphere in units of Earth ocean equivalent content of hydrogen (EO_H) with respect to the ratio \( L_{\text{XUV}}/L_0 \). This behaviour is plotted for two cases: a stoichiometric mixture of hydrogen and oxygen atoms \( X_O = X_H/2 = 1/3 \) and a mixture slightly depleted in hydrogen \( X_O = 2X_H/2 = 2/3 \). We can see that the mass-loss is a monotonous function of the total XUV luminosity, and for both cases it saturates much below our baseline case. For a stoichiometric mixture, at a ratio \( L_{\text{XUV}}/L_0 \sim 0.13 \), the oxygen atoms start to be dragged along therefore consuming energy. For a mixture depleted in hydrogen, oxygen atoms start to be dragged along for lower incoming XUV luminosity \( L_{\text{XUV}}/L_0 \sim 0.075 \).

However, here, for \( L_{\text{XUV}} = L_0 \), we find that one oxygen atom is lost for about five hydrogen atoms: \( r_f = F_0/F_H = 0.20 \). To conclude, for a X-ray luminosity of \( 10^{25.4} \text{ erg s}^{-1} \), there is no stoichiometric loss of hydrogen and oxygen. However, the situation is not as catastrophic as it would be if only hydrogen escaped. In the following, we give the hydrogen lost by the planet. We assume that \( r_f \) is constant with time for a given value of the XUV flux, which is equivalent to assume an infinite reservoir of water. With a finite water reservoir one has to account for the evolution of the O/H ratio. As it makes the result depend on the initial reservoir, we choose to maximize the effective water loss by using the value of \( r_f \) calculated for a ratio \( X_O = X_H/2 \). The hydrogen mass-loss is thus given by

\[ M_H = m \frac{m_H}{m_H + r_f m_O}, \]

where \( m \) is obtained from equation (3) and is given in units of the mass of hydrogen in one Earth ocean (EO_H). Hydrogen is the limiting element for the recombination of water, so that the remaining content of hydrogen in EO_H actually represents the ocean portion available for precipitation once in the HZ.

According to equation (6), \( r_f \) depends on the gravity of the planet. In the following, we also calculate the hydrogen loss from planets of 0.1 and 5 M_\oplus. Computing the hydrogen loss for these cases shows us that the higher the mass the lower is \( r_f \). For \( L_{\text{XUV}} = L_0 \), we find that \( r_f \sim 0.45 \) for the 0.1 M_\oplus planet (meaning that the loss is quasi-stoichiometric) and \( r_f = 0 \) for the 5 M_\oplus planet (meaning that the only hydrogen atoms escape).
4 WATER LOSS OF PLANETS IN THE UCD HABITABLE ZONE

Using the estimation of $\epsilon$ as a function of XUV flux (Fig. 2), the estimations of $r_F$ as calculated in the previous section and the equations of Section 3, we can now estimate the loss of hydrogen from planets around UCDs.

Fig. 4(a) shows the evolution of the hydrogen loss from an Earth-mass planet orbiting a 0.04 M$_\odot$ BD as a function of both time and orbital radius (assumed to remain constant). We assume that the X-ray luminosity scales as $10^{-5} L_{bol}$ and we calculate $\epsilon$ and $r_F$ accordingly (typically, for a planet at 0.013 au, $\epsilon$ varies between 0.045 and 0.111 as the XUV flux decreases and $r_F$ decreases from 0.43 to 0.10). Let us consider that the planet is located at 0.013 au from a 3-Myr-old BD. Fig. 4(a) shows that it would lose only 0.48 EO$_H$ in the 156 Myr before entering the HZ (vertical red dashed line). This time is ~3 Myr for a BD of 0.01 M$_\odot$ and ~1180 Myr for a dwarf of 0.08 M$_\odot$. The calculations were done for both cases: $L_X/L_{bol} = 10^{-5}$ (red symbols) and $L_X = 10^{25.4}$ erg s$^{-1}$ (blue symbols). As before, $\epsilon$ and $r_F$ were calculated consistently for each planet and for the two X-ray-luminosity assumptions.

We find that planets orbiting more massive UCDs lose more water. This is mainly because of the much longer time spent by those planets interior to the HZ. Planets at 0.013 au around BDs of mass 0.01 M$_\odot$ lose less than 0.04 EO$_H$, irrespective of their mass. Planets at 0.013 au around BDs of mass 0.05 M$_\odot$ lose less than 2 EO$_H$, irrespective of their mass. Planets at 0.013 au around UCDs of mass 0.08 M$_\odot$ lose more than 2 EO$_H$, irrespective of their mass.

We find that higher mass planets lose their water at a higher rate than lower mass ones. This is due to the effect of gravity on the cross-over mass that makes $r_F$ smaller for a higher gravity. In other words, too high a gravity prevents the loss of oxygen and thus enhances the loss of hydrogen (which is not directly affected by gravity, e.g. Luger & Barnes 2015). Consequently, throughout the evolution, we expect more massive planets to lose more than low-mass planets. For example, assuming $L_X/L_{bol} = 10^{-5}$, we find that the 5 M$_{\oplus}$ planet orbiting a UCD of 0.08 M$_\odot$ loses 6.7 EO$_H$ before reaching the HZ, while the 1 M$_{\oplus}$ loses only 3.2 EO$_H$ and the 0.1 M$_{\oplus}$ only 2.0 EO$_H$.

Assuming $L_X/L_{bol} = 10^{-5}$, we find that 1 M$_{\oplus}$ planets orbiting at 0.013 au around BDs with masses smaller than 0.06 M$_\odot$ lose less than 1 EO$_H$ before reaching the HZ and 1 M$_{\oplus}$ planets orbiting BDs of mass $\lesssim 0.07$ M$_\odot$ lose less than 2 EO$_H$ before reaching the HZ. Whatever the mass of the UCD, low-mass planets ($M_p \lesssim 1$ M$_{\oplus}$) lose less than 3.2 EO$_H$ before reaching the HZ. Whatever the mass of the UCD, whatever the mass of the planet and the XUV-luminosity assumption, all planets lose less than 9 EO$_H$ before reaching the HZ.

Fig. 6 shows the hydrogen loss as a function of the planet’s orbital distance and mass of host UCD. The black lines represent different hydrogen-loss levels (1, 2, 10 EO$_H$) and the white lines represent levels of time the planet spends in the HZ (as computed as in Fig. 1). The closer the planet and the more massive the UCD, the more hydrogen is lost. The closer the planet and the more massive the UCD, the more time the planet spends in the HZ. However for the more massive UCD we consider (as can be seen in Fig. 1 for the UCD of 0.08 M$_\odot$), the planets on the closest orbits are always interior to the HZ and thus stay in a runaway phase during all the time of the evolution (10 Gyr). In Fig. 6, these planets are separated from the rest by the blue dashed line. They can lose up to 160 EO$_H$. There is a compromise to be found between the hydrogen loss and the time the planet spends in the HZ: planets around low-mass BDs lose little hydrogen but they stay for a short time in the HZ, planets around the higher mass UCDs considered here spend a longer time in the HZ but they lose more hydrogen prior to entering the HZ. The shaded regions in Fig. 6 show an interesting parameter space for each planet and XUV emission hypothesis: the planets in these regions lose less than 1 EO$_H$ before entering the HZ and spend more than 1 Gyr in the HZ. Planets with a similar or larger water content as the Earth would thus enter the HZ with enough water to form oceans and as they spend a long time in the HZ, this gives time for life to eventually appear and modify the environment (Bolmont et al. 2011). For example,
for an Earth-mass planet and assuming $L_X/L_{bol} = 10^{-5}$, we find that the planets around UCDs more massive than $\sim 0.035 \, M_{\odot}$ and farther away than 0.007 au fulfil these conditions. Of course, when considering higher mass UCDs, the minimum orbital distance increases: a planet around a 0.08 $M_{\odot}$ UCD has to be at farther away than $\sim 0.02$ au to fulfil the conditions. If we consider softer constraints, for example cases for which the planets lose less than 2 $E_{O_{\odot}}$ and spend more than 500 Myr in the HZ, the parameter space gets much bigger: for example, Earth-mass planets as close as 0.005 au around a 0.02 $M_{\odot}$ BD fulfil these conditions. However, these very close-in planets could be in danger of falling on to the BD: they could be interior to the corotation radius (see Fig. 1 and Bolmont et al. 2011). If we consider 5 $M_{\odot}$ planets, the parameter space corresponding to a loss $\leq 1 \, E_{O_{\odot}}$ and a time in the HZ $\geq 1$ Gyr shrinks towards the higher UCD masses and bigger orbital distances. If we consider 0.1 $M_{\odot}$ planets, the parameter space corresponding to a loss $\leq 1 \, E_{O_{\odot}}$ and a time in the HZ $\geq 1$ Gyr extends towards the lower UCD masses and smaller orbital distances. We thus can conclude that with favourable atmospheric conditions and reasonable water content (a few oceans), Earth-mass planets between 0.01 and 0.04 au orbiting UCDs of mass 0.04–0.08 $M_{\odot}$ would be good targets for the characterization of a potentially habitable planet.

5 IMPLICATION FOR THE TRAPPIST-1 PLANETS

The three planets of the TRAPPIST-1 system (Gillon et al. 2016) are Earth-sized planets, and thus probably rocky (Weiss & Marcy 2014; Rogers 2015). They orbit a M8-type dwarf of 0.080 $\pm$ 0.009 $M_{\odot}$; TRAPPIST-1b is located at $a_b = 0.011$ au, TRAPPIST-1c at $a_c = 0.015$ au. The orbit of TRAPPIST-1d is poorly constrained, however it is farther away than $a_d = 0.022$ au. The irradiation of the planets are, respectively, 4.25 and 0.02–1 $S_{\odot}$, where $S_{\odot}$ is the insolation received by the Earth. Therefore, TRAPPIST-1d could be in the HZ. The age of the system has been estimated to be more than 500 Myr. The structural evolution grids we use in this paper for a dwarf star of 0.08 $M_{\odot}$ (Chabrier & Baraffe 1997) show that the luminosity and radius of TRAPPIST-1 correspond to a body of $\sim 400$ Myr, which is lower than the estimated age of the system. This is consistent with the fact that evolution models seem to underestimate the luminosity of low-mass objects (Chabrier, Gallardo & Baraffe 2007). However, we explored the mass range allowed by the observations and found that a dwarf star of 0.089 $M_{\odot}$ can reproduce the characteristics of TRAPPIST-1 at an age of $\sim 850$ Myr.

\footnote{TRAPPIST-1 is therefore not a BD but a very low-mass star.}
Figure 6. Hydrogen loss (black contour lines) as a function of the mass of the UCD and the orbital distance of the planet. Panels (a) corresponds to $L_X = 10^{25.4}$ erg s$^{-1}$ and panels (b) corresponds to $L_X/L_{bol} = 10^{-5}$. The blue lines correspond from left to right to time spent in the HZ of 500 Myr and 1 Gyr. The dashed blue line corresponds to the limit where the planets never reach the HZ because the dwarf initiated the fusions of hydrogen preventing the inner edge of the HZ to sweep in towards very small orbital distances (see Fig. 1). The blue shaded areas represent two interesting parameter spaces: the planets in the light blue area lose less than $2 EOH$ before reaching the HZ and they will spend more than 500 Myr in it, the planets in the dark blue area lose less than $1 EOH$ before reaching the HZ and they will spend more than 1 Gyr in it.
Fig. 7 shows the evolutionary tracks we used to simulate the luminosity evolution of TRAPPIST-1. We interpolated the values of radius, luminosity and effective temperature between the evolutionary tracks of a 0.08 M$_\odot$ dwarf and a 0.1 M$_\odot$ dwarf (Chabrier & Baraffe 1997). Fig. 7 shows that the characteristics of the star – radius, luminosity and effective temperature – can be reproduced with our interpolated tracks for ages between 800 and 900 Myr, which is compatible with the estimation of the age of the star made by Gillon et al. (2016).

We use here two different assumptions to calculate the HZ inner edge: $S_p = 0.9 S_\oplus$, which corresponds to the inner edge for a non-synchronized planet (Kopparapu et al. 2013) and $S_p = 1.5 S_\oplus$ which corresponds to the inner edge for a synchronized planet (Yang, Cowan & Abbot 2013). Following this model, the two inner planets of TRAPPIST-1 always stay interior to the HZ. As the orbit of planet d is poorly constrained, we considered three different orbits: 0.022 au (the closest one), 0.058 au (the most probable one) and 0.146 au (the farthest one). A planet at 0.022 au enters the HZ corresponding to $S_p = 1.5 S_\oplus$ at an age of 393 Myr [later called $T_{HZ}(1.5 S_\oplus)$]. However, it never enters the HZ corresponding to $S_p = 0.9 S_\oplus$. For a planet at 0.058 au, $T_{HZ}(1.5 S_\oplus) = 29$ Myr and $T_{HZ}(0.9 S_\oplus) = 58$ Myr. For a planet at 0.146 au, $T_{HZ}(1.5 S_\oplus) = 3.2$ Myr and $T_{HZ}(0.9 S_\oplus) = 5.4$ Myr. If we had considered more massive stars than allowed by Gillon et al. (2016), the entry in the HZ would have been postponed by at least a few tens of million years increasing the period of time the planet spends in the runaway phase.

To calculate the mass-loss from the planets of the TRAPPIST-1 system, we assumed different XUV emissions. As explained in Section 3.2, TRAPPIST-1 is part of the transition population between early M type and late M, early L. In order to treat the whole XUV range possible, we assumed the two different XUV luminosity measured by Wheatley et al. (2016):

$$L_{X}/L_{bol} = 10^{-3.7} \text{ and } L_{X}/L_{bol} = 10^{-3.4}$$

Observational studies (e.g. Cook et al. 2014; Williams et al. 2014) indicate a significantly large scatter at spectral type M8, with values ranging between $L_{X}/L_{bol} = 10^{-5}$ and $10^{-3}$ in quiescence. Cook et al. (2014) mention another analogue of TRAPPIST-1, LP 412-31, which has a quiescent emission of $10^{27.2}$ erg s$^{-1}$ or $L_{X}/L_{bol} = 10^{-3.1}$. Furthermore, using XMM–Newton observations, Wheatley et al. (2016) measured recently for TRAPPIST-1 $L_{X}/L_{bol} = 10^{-3.7}$ to

3 Its bolometric luminosity $L_{bol}/L_\odot \sim 10^{-3.29}$ is close to the luminosity of TRAPPIST-1 ($L_{bol}/L_\odot \sim 10^{-3.28}$), its $V\sin i$ of 8 km s$^{-1}$ (Reid et al. 2002; Newton et al. 2016) is also close to TRAPPIST-1’s $\sim 6$ km s$^{-1}$. 

MNRAS 464, 3728–3741 (2017)
10^{-3.4}, which is significantly higher than the value we adopted for the UCDs of the previous sections.

(2) \( L_X/L_{\text{bol}} = 10^{-5} \)

This is what we used for UCDs in the previous sections. As the measurements of Wheatley et al. (2016) could be due to a flare, we consider this much lower flux. This also corresponds to an analogue of TRAPPIST-1: the M8 dwarf VB 10.\(^4\) Observations of VB 10 by Fleming, Giampapa & Schmitt (2000) showed that the quiescent emission was \( L_X = 10^{-6.0} L_{\text{bol}} \) and the flaring emission was \( L_X = 10^{-2.8} L_{\text{bol}} \). Later, Berger et al. (2008) measured \( L_X = 10^{-3.0} L_{\text{bol}} \) for the quiescent emission and \( L_X = 10^{-4.1} L_{\text{bol}} \) during flaring events. Finally, Williams et al. (2014) and Cook et al. (2014) found that the quiescent emission of VB 10 was \( L_X = 10^{-5.1} L_{\text{bol}} \) and that the flaring emission was \( L_X = 10^{-4.4} L_{\text{bol}} \).

We used the method described in Section 3.1, using an efficiency \( \epsilon \) based on the hydrodynamical simulations of Section 3.3. We assumed an Earth-like composition to compute the masses of the planets (Fortney, Marley & Barnes 2007) and we calculated \( r_L \) following the method given in Section 3.4 for the three different XUV luminosity assumptions and for the different planets of the system. We assumed that the semimajor axes of the planets remain constant throughout the evolution.

Fig. 8 shows the hydrogen loss for the planets of the system for the three different XUV-luminosity trends as a function of time. Table 1 summarizes the results. For \( L_X/L_{\text{bol}} = 10^{-5} \), we considered that \( L_{XUV} = 5L_X \), as in Section 4. However, for \( L_X/L_{\text{bol}} = 10^{-3.4} \) and \( L_X/L_{\text{bol}} = 10^{-3.7} \), we used the value of Wheatley et al. (2016): \( L_{XUV} = 1.78L_X \). For \( L_X/L_{\text{bol}} = 10^{-5} \), we find that planet b loses less than 4 EO\(\text{H}_2\) and planet c loses less than 5 EO\(\text{H}_2\) at the age of the system. However, considering a higher XUV flux, this limit goes up to 13.5 EO\(\text{H}_2\) for planet b and 9.5 EO\(\text{H}_2\) for planet c. Unless those planets have a big water content, they are therefore likely to be desiccated.

For planet d, due to the high uncertainty on its orbit, we find that at worst it could lose almost 7 EO\(\text{H}_2\) for an orbital separation of 0.022 au (assuming \( L_X/L_{\text{bol}} = 10^{-3.4} \) and that the planet never reaches the HZ). For \( L_X/L_{\text{bol}} = 10^{-5.0} \), a planet d at 0.022 au loses more hydrogen than planet c at late ages. This is due to a combination of the effect of gravity on the cross-over mass (planet d being bigger than planet c, its \( r_L \) is smaller) and XUV flux that is lower for planet d, which means that the efficiency \( \epsilon \) is bigger.

However, considering TRAPPIST-1d is on the more probable orbit, at 0.058 au, we find that it loses between 0.06 and 0.41 EO\(\text{H}_2\).

---

\( ^4 \) Its bolometric luminosity \( L_{\text{bol}}/L_{\odot} \sim 10^{-3.3} \) is close to the luminosity of TRAPPIST-1 (\( L_{\text{bol}}/L_{\odot} \sim 10^{-3.28} \)), its \( V \sin i \) of 6.5 km s\(^{-1}\) is also close to TRAPPIST-1’s \( \sim 6 \) km s\(^{-1}\). Their radii are also similar within a few per cent.
It loses much less than if it was at 0.022 au because it is much farther away and enters the HZ much earlier. If TRAPPIST-1d is at 0.146, it loses less than 0.01 EO\textsubscript{H}. As hydrogen escapes faster than oxygen, mass-loss results in an oxygen build up in the atmosphere (e.g. Luger & Barnes 2015). We estimate the O\textsubscript{2} pressure in the atmosphere of the different planets (see Table 1). The pressure of O\textsubscript{2} can be as high as 500 bar for a planet d at 0.022 au. It is even higher than the O\textsubscript{2} pressure for the two inner planets, because as the XUV flux planet d receives is lower than for planets b and c, its $\rho_1$ is smaller and it therefore loses much less oxygen than the two inner planets. For a planet d at 0.058 au up to 30 bar of O\textsubscript{2} can build up in the atmosphere by the time it reaches the HZ.

The orbit of TRAPPIST-1d is not well constrained, but there is a high probability that it is in the HZ. This calculation shows that there is a non-negligible probability that this planet was able to retain a high fraction of an eventual water reservoir of one Earth ocean, which makes it a very interesting astrobiology target.

Additional measurements of TRAPPIST-1’s X-ray luminosity are needed in order to establish whether the values of Wheatley et al. (2016) correspond to a flare or not (a discussion about the quantitative effect of flares can be found in Section 6.3). Besides, what might give us a deeper insight of the escape mechanisms for TRAPPIST-1’s planets will be the characterization of the atmospheres of the three planets. Indeed, Belu et al. (2013) showed that the atmosphere of the planets of TRAPPIST-1 could be characterizable with facilities such as JWST. The observation of these planets could therefore provide us information on water delivery during the formation processes and their capacity to retain water.

6 DISCUSSION

6.1 Why this result likely overestimate the loss

In this section, we show that the thought process we performed in the previous section, both following the standard way of computing mass-loss (as in Barnes & Heller 2013) and using simple radiation-hydrodynamics calculations (as in Owen & Alvarez 2016) may actually be overestimating the mass-loss.

(i) The time of the disc dispersal we consider here might be too short for such low-mass objects. The evolution of discs around UCDs is not well constrained, however it is reasonable to assume they dissipate between 3 and 10 Myr (discs around low-mass stars tend to have longer lifetimes, e.g. Pascucci et al. 2009; Liu et al. 2015; Downes et al. 2015). Discs around UCDs could very well dissipate at an age of 10 Myr. As young UCDs are brighter than old UCDs, a later dissipation of the disc would mean that a planet is exposed for less time and to a weaker XUV radiation, meaning that the planet would lose less water than calculated in this work. For example, a 1 M\textsubscript{☉} planet orbiting a 0.06 M\textsubscript{☉} BD at 0.013 au would only lose 0.41 EO\textsubscript{H} by the time it reaches the HZ if the disc dissipates at 10 Myr (instead of 0.48 EO\textsubscript{H} if the disc dissipates at 3 Myr, see Fig. 5, for $L_\text{bol}/L_{\text{bol, bol}} < 10^{-5}$). And a planet orbiting a 0.06 M\textsubscript{☉} BD at 0.013 au would lose only 1.06 EO\textsubscript{H} if the disc dissipates at 10 Myr (instead of 1.15 EO\textsubscript{H} if the disc dissipates at 3 Myr). Under this assumption of a longer lived protoplanetary disc, planets can therefore keep slightly more water.

(ii) Water vapour photolysis is required to feed the loss in hydrogen atoms and is produced by FUV radiation (100–200 nm). UCDs are too cool to produce a significant photospheric FUV flux and H\textsubscript{2}O-photolysing radiation is likely to be restricted to the Lyman $\alpha$ emission. Recent observations of 11 M-dwarfs by France et al. (2016) showed that the estimated energy flux in the Lyman $\alpha$ band is equal to the flux in the XUV range. Using this constraint, we can estimate the quantity of hydrogen produced by photodissociation. Fig. 9 shows the quantity of hydrogen lost according to our calculations of Section 4 and the quantity of hydrogen available.

If all the incoming FUV photons do photolysate H\textsubscript{2}O molecules with a 100 per cent efficiency ($\epsilon_\alpha = 1$) and all the resulting hydrogen atoms remain available for the escape process then photolysis does not appear to be limiting the loss process. The production rate of hydrogen atoms exceeds the computed thermal loss assuming a hydrogen and oxygen mixture. In reality, however, only a fraction of the incoming FUV actually results in the loss of a hydrogen atom. Part of the incoming photons are absorbed by other compounds (in particular hydrogen in the Lyman $\alpha$ line) or backscattered to space. Then, products of H\textsubscript{2}O photolysis (mainly OH and H) recombine through various chemical pathways. If the efficiency $\epsilon_\alpha$ is less than about 23 per cent then the loss rate becomes photolysis limited. Although efficiency calculations would require detailed FUV radiative transfer and photochemical schemes, we can safely argue that efficiencies much lower than 23 per cent can be expected.

It is important to stress that the loss is likely to be photolysis limited, which would allow us to calculate upper limits of the loss without the need of complex thermal and non-thermal escape models. At this point the FUV flux, which is the key input for H\textsubscript{2}O photolysis, is only estimated based on the XUV/FUV ratio measured on earlier type stars. Measuring the FUV of UCDs could allow us to put strong constraints on the water erosion on their planets.

(iii) The XUV flux considered here might be much higher than what is really emitted by UCDs. Indeed, all Chandra observations of X-ray emissions of low-mass objects (e.g. Berger et al. 2010; Williams et al. 2014) are actually non-detection for the UCD range. New estimations from Osten et al. (2015) show that upper limits

Table 1. Lost hydrogen in EO\textsubscript{H} and corresponding O\textsubscript{2} pressure for the TRAPPPIST-1 planets at the time they enter the HZ (with the two assumptions about the inner edge). The numbers in bold correspond to cases for which the planet never reaches the HZ, the hydrogen loss is then given for the age of the star ($\sim$850 Myr, according to our model). The two values indicated correspond to $t_0 = 10$ Myr and $t_0 = 3$ Myr.

| SMA (au) | $L_X/L_{bol}$ $= 10^{-3.4}$ | $T_{bol}$ (0.9 S\textsubscript{⊕}) | $T_{bol}$ (1.5 S\textsubscript{⊕}) | Hydrogen loss (EO\textsubscript{H}) | Hydrogen loss (EO\textsubscript{H}) |
|---------|--------------------------|------------------|------------------|-------------------------------|-------------------------------|
| T1-b    | 0.0111                  | 12.76–13.18      | 8.96–9.28        | 3.61–3.73                     | 418–422                      |
| T1-c    | 0.01522                 | 9.19–9.53        | 6.39–6.63        | 2.60–2.69                     | 345–348                      |
| T1-d    | 0.022                   | 6.50–6.78        | 3.70–3.93        | 4.85–5.00                     | 428–422                      |
| T1-d    | 0.058                   | 0.32–0.41        | 0.15–0.24        | 0.24–0.30                     | 28–32                        |
| T1-d    | 0.146                   | <0.01            | <0.002           | <0.01                         | <14                           |
| T1-d    | 0.058                   | 0.15–0.24        | 0.15–0.24        | 0.24–0.30                     | 28–32                        |
| T1-d    | 0.146                   | <0.01            | <0.002           | <0.01                         | <14                           |
found for the X-ray luminosity for the object Luhman 16AB (WISE J104915.57–531906.1, L7.5 and T0.5 spectral types) are lower than what we used in this study: $L_X < 10^{25}$ erg s$^{-1}$ or $L_X/L_{bol} < 10^{-5.7}$. Besides, Mohanty et al. (2002) show that in BDs’ cool atmospheres the degree of ionization is very low so it is very possible that the mechanisms needed to emit X-rays are not efficient enough to produce the fluxes considered in this work. In which case, the computed mass-loss would be lower than what we calculated here.

(iv) We find that the planets might lose several $E_{OH}$. Therefore, depending on the initial water content, some of them are in danger to be desiccated. The close-in planets we consider may not have formed in situ but migrated from the outer regions of the disc and could have accumulated a large amount of water. Both on the observational and theoretical side, it has been shown that planets could even have a large portion of their bulk made out of water (ocean planets, hypothesized by Kuchner 2003; Léger et al. 2004; Ogihara & Ida 2009). For example, Kaltenegger, Sasselov & Rugheimer (2013) have identified Kepler-62e and 62f to be possible ocean planets. Furthermore, as discussed in Marty (2012), a large part of water can be trapped in the mantle to be released by geological events during the evolution of the planet, allowing a replenishment of the surface water content.

(v) Johnson, Volkov & Erwin (2013) showed using molecular-kinetic simulations that the mass-loss saturates for high incoming energy, which could mean that in our case the mass-loss would be smaller than what we calculated. However, their results should be applied to our specific problem in order to verify this statement.

6.2 Why this result is different from previous ones

Unlike Barnes & Heller (2013), we find that planets in the HZs of UCDs should in most cases be able to retain a non-negligible portion of their initial reservoir of water. The main differences between Barnes & Heller (2013) and our work are the following. First, they used for the XUV radiation an observed upper limit for early-type M-dwarfs (Pizzolato et al. 2003, which was the only available study at the time) for which the XUV luminosity scales as $10^{-3}$ times the bolometric luminosity. We used here more recent estimates of X-ray emission of later type dwarfs, which show that UCDs emit much less X-rays than earlier type M-dwarfs (Berger et al. 2010; Williams et al. 2014; Osten et al. 2015). Secondly, in addition to the standard method used in Barnes & Heller (2013) and Luger & Barnes (2015), we also improved the robustness of our results obtained with an improved energy-limited escape formalism using a better estimate of the fraction of the incoming energy that is transferred into gravitational energy through the mass-loss ($\epsilon$) obtained with 1D radiation-hydrodynamic mass-loss simulations (Owen & Alvarez 2016). Thirdly, Barnes & Heller (2013) used a larger XUV cross-section for the planets. However, using our hydrodynamical model, we found that for such small planets the XUV cross-section is very similar to the radius of the planet and only causes a difference of a few per cent in the quantity of water lost. Fourthly, they considered a loss of hydrogen atoms, while in this work we estimated the ratio of the escape fluxes of both hydrogen and oxygen atoms ($r_y$). We found that in most of the configurations considered here, oxygen atoms are dragged away by the escaping hydrogen atoms, which is more favourable for water retention.

6.3 The effect of flares

We only consider here quiescent energetic emissions. However, BDs could emit energetic flares for a significant fraction of their lifetime in the H$_{\alpha}$ emission line and in the U-band (Schmidt et al. 2014; Schmidt 2014). This would also endanger the survival of a water reservoir. Gizis et al. (2013) showed that these flares can be as frequent as one to two times a month (e.g. the L1 dwarf W1906+40). W1906+40 experienced a white flare during ~2 h, which released an energy of $10^{29}$ erg (in a band 400–900 nm). Let us consider here that the flare released in the XUV range 20 per cent of the energy it released in the 400–900 nm band (this proportion has been measured for Sun flares in Kretzschmar et al. 2011). This flare would then correspond to an energy ~11 times what we considered for the quiescent emission in the case of the constant XUV emission ($L_X = 10^{25.4}$ erg s$^{-1}$). Using the equation (3), we find that if such a flare happened for 2 h every months (as could be the case for W1906+40), would reduce slightly the lifetime of the water reservoir. For example, a 1 $M_\oplus$ planet at 0.01 au orbiting a UCD of $M_{BD} = 0.04 M_\odot$ would lose 0.191 $E_{OH}$ instead of 0.189 $E_{OH}$ before reaching the HZ at ~60 Myr (assuming $L_X = 10^{25.4}$ erg s$^{-1}$, blue squares on Fig. 5) a. A 1 $M_\oplus$ planet at 0.01 au orbiting a UCD of $M_{BD} = 0.08 M_\odot$ would lose 0.899 $E_{OH}$ instead of 0.890 $E_{OH}$ before reaching the HZ at ~300 Myr. Taking into account the flares therefore does not significantly change the results.

6.4 Water retention does not equal habitability

Water retention is not synonymous with habitability. Given that BD’s HZs are very close-in, HZ planets feel strong tidal forces. This may affect their ability to host surface liquid water. For example, a lone planet would likely be in synchronous rotation. One can imagine that all liquid water might condense on to the night side (cold trap). However, this can be avoided if the atmosphere is dense enough to efficiently redistribute the heat (e.g. Leconte et al.
In multiple-planet systems, a HZ planet’s eccentricity can be excited and lead to significant tidal heating (Barnes et al. 2009, 2010; Bolmont et al. 2013; Bolmont, Raymond & Selsis 2014). In some cases, tidal heating could trigger a runaway greenhouse state (Barnes & Heller 2013). In other situations, such as in the outer parts of the HZ or even exterior to the HZ, tidal heating may be beneficial by providing an additional source of heating and perhaps even by helping to drive plate tectonics (Barnes et al. 2009).

7 CONCLUSIONS

Considering a very unfavourable scenario for water retention – complete dissociation of water molecules – and assuming different values for the X-ray luminosity of the UCDs, we find regions of parameter space (mass of UCD versus orbital distance of the planets) for which planets lose less than a few EO_H (here equal to the hydrogen reservoir in one Earth ocean) before reaching the HZ and can also spend a long time in the HZ. When reaching the HZ, the remaining hydrogen can recombine with the remaining oxygen to form water molecules that can then condense. The longer the planet spends in the HZ, the more time life has to eventually appear, evolve and be observable. Bolmont et al. (2011) showed that the more massive the BD, the longer a close-in planet spends in the HZ. The low-mass BDs will always suffer from the fact that they cool down very fast and that at best, planets spend a few 100 Myr in the HZ. Even though this could be enough time for life to appear, its potential detectability would be a rare event.

This work therefore shows that there is a potential sweet spot for life around UCDs: planets between 0.01 and 0.04 au orbiting BDs of masses between ∼0.04 and 0.08 M⊙ (assuming L_X/L_bol = 10⁻⁵ or L_X = 10²⁶.4 erg s⁻¹) lose less than 1 EO_H while in runaway and then spend a long time in the HZ (≥ 1 Gyr, according to Bolmont et al. 2011). Considering a higher X-ray luminosity (L_X/L_bol = 10⁻⁴.⁵ or L_X = 10²⁶ erg s⁻¹), this sweet spot shifts towards higher orbital distances and higher UCD masses: planets between ∼0.02 and 0.04 au orbiting UCDs of mass between ∼0.06 and 0.08 M⊙ lose less than 1 EO_H while in runaway and then spend a long time in the HZ. Of course, if one of the mechanisms considered here does not take place, or if the real XUV flux of BDs is lower than the upper value we considered, as we discussed in the previous Section 6.1, the sweet spot for life could widen towards the smaller orbital distances.

We also investigated hydrogen losses in the Trappist-1 system (Gillon et al. 2016). Assuming a X-ray quiescent emission comparable to a similar star as TRAPPIST-1 (VB 10), we find that the two inner planets of the system TRAPPIST-1 (Gillon et al. 2016) might have lost up to 4 EO_H, but that the third planet has lost less than 3 EO_H. Assuming a X-ray quiescent emission as high as Wheatley et al. (2016), we find that if planet d has an orbital distance of 0.058 au (the most probably one from Gillon et al. 2016) it would have only lost at worst ∼0.40 EO_H. If the X-ray luminosity of TRAPPIST-1 measured by Wheatley et al. (2016) is confirmed, the observation of the presence of water on the two inner planets would actually provide us information about the planets initial water content.

Despite the lack of knowledge about escape mechanisms, in particular about the way hydrogen and oxygen jointly escape (or not), we find that there are possibilities that planets around UCDs might arrive in the HZ with an important water reservoir even without invoking an initial water reservoir larger than the Earth. As shown in Section 6.1, there might be even more possibilities if the loss of hydrogen is photolysis limited, which would happen if the efficiency of this process is below 20 per cent. Furthermore, planets in the HZs of BDs may be easy to detect in transit due to their large transit depths and short orbital periods (at least for sufficiently bright sources; Belu et al. 2013; Triaud et al. 2013). Given their large abundance in the Solar neighbourhood (∼1300 have been detected to date; see http://DwarfArchives.org), such planets may be among the best nearby targets for atmospheric characterization with the JWST. In particular, the planets of TRAPPIST are an ideal laboratory to test the mechanisms of mass-loss.

ACKNOWLEDGEMENTS

The authors would like to thank Rory Barnes and René Heller for bringing this subject to their attention. The authors would also like to thank Rodrigo Luger for useful comments and for helping improve our manuscript. The authors also thank the referee for the useful comments on the manuscript.

EB acknowledges that this work is part of the F.R.S.-FNRS ExtraOdynHa research project. The work of EB was supported by the Hubert Curien Tournesol Program. IR acknowledges support from the Spanish Ministry of Economy and Competitiveness (MINECO) through grant ESP2014-57495-C2-2-R. FS acknowledges support from the Programme National de Planétologie (PNP). SNR thanks the Agence Nationale pour la Recherche for support via grant ANR-13-BS05-0003-002 (project MOJO). JEO acknowledges support by NASA through Hubble Fellowship grant HST-HF2-51346.001-A awarded by the Space Telescope Science Institute, which is operated by the Association of Universities for Research in Astronomy, Inc., for NASA, under contract NAS 5-26555. MG is Research Associate at the F.R.S.-FNRS.

REFERENCES

Andreassee chev A., Scala J., 2004, in Norris R., Stoo tan F., eds, Proc. IAU Symp. Vol. 213, Bioastronomy 2002: Life Among the Stars. Astron. Soc. Pac., San Francisco, p. 115
Barnes R., Heller R., 2013, Astrobiology, 13, 279
Barnes R., Jackson B., Greenberg R., Raymond S. N., 2009, ApJ, 700, L30
Barnes R., Jackson B., Greenberg R., Raymond S. N., Heller R., 2010, in Coudé du Foresto V., Gelino D. M., Ribas I., eds, ASP Conf. Vol. 430, Pathways Towards Habitable Planets. Astron. Soc. Pac., San Francisco, p.133
Barstow J. K., Irwin P. G. J., 2016, MNARS, 461, L92
Belu A. R. et al., 2013, ApJ, 768, 125
Berger E. et al., 2008, ApJ, 676, 1307
Berger E. et al., 2010, ApJ, 709, 332
Berta Z. K. et al., 2012, ApJ, 747, 35
Bolmont E., Raymond S. N., Leconte J., 2011, A&A, 535, A94
Bolmont E., Selsis F., Raymond S. N., Leconte J., Hersant F., Maurin A.-S., Pericau J. E., 2013, A&A, 556, A17
Bolmont E., Raymond S. N., Selsis F., 2014, in Ballet J., Martins F., Bournaud F., Monier R., Reylé C., eds, SF2A-2014: Proc. Annual Meeting of the French Society of Astronomy and Astrophysics, p. 63
Chabrier G., Baraffe I., 1997, A&A, 327, 1039
Chabrier G., Gallardo J., Baraffe I., 2004, in Norris R., Stootman F., eds, Proc. IAU Symp. Vol. 213, Bioastronomy 2002: Life Among the Stars. Astron. Soc. Pac., San Francisco, p. 115
Cook B. A., Williams P. K. G., Berger E., 2014, ApJ, 785, 10
Downes J. J. et al., 2015, MNRAS, 450, 3490
Erkaev N. V., Kulikov Y. N., Lammer H., Selsis F., Langmayr D., Jaritz G. F., BIermaat H. K., 2007, A&A, 472, 329
Fleming T. A., Giampapa M. S., Schmitt J. H. M. M., 2000, ApJ, 533, 372
Fortney J. J., Marley M. S., Barnes J. W., 2007, ApJ, 659, 1661
France K. et al., 2016, ApJ, 820, 89
This paper has been typeset from a TeX/LaTeX file prepared by the author.