Intrinsic electron-glass effects in strongly-localized thallium-oxide films

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Abstract

Transport measurements made on films of thallium-oxide (n-type semiconductor) are presented and discussed. The focus in this work is on the strongly-localized regime where charge transport is by variable-range-hopping. It is demonstrated that, at liquid-helium temperatures, these films exhibit all the characteristic features of intrinsic electron-glasses. These include a slow (logarithmic in time) conductance-relaxation that may be induced by any of the following protocols: Quench-cooling from high temperatures, sudden change of gate-voltage, exposure to infrared radiation, and stressing the system with a non-Ohmic field. Experimental evidence for glassy effects, however, has been somewhat scarce. Intrinsic EG effects were found in several systems but remarkably none was reported in lightly-doped semiconductors. By ‘intrinsic EG’ we mean that the effects appear systematically for a given substance independently of the way the sample was prepared. It has been conjectured that the reason for the absence of intrinsic EG effects in lightly-doped semiconductors is their inherently short relaxation-time, which makes it hard to resolve these effects by transport measurements. The short relaxation time of semiconductors was alleged to be due to their low carrier-concentrations. This has been supported by a recent experiment on phosphorous-doped silicon where ultra-fast relaxation was found. Conductance relaxations that persist for many seconds, and memory effects characteristic of intrinsic electron-glass, seem to be peculiar to systems with $n>5\times10^{19}$cm$^{-3}$.

Intrinsic electron-glass effects were observed in films of crystalline indium-oxide (In$_2$O$_{3-x}$), several versions of amorphous indium-oxide (In$_x$O), and, in ultra-thin films of beryllium. In all these materials the carrier-concentration was measured by Hall effect and verified to be in the high-$n$ limit.

In this work we report on the low temperature transport properties of thallium-oxide, which is n-type semiconductor with high carrier-concentration. The microstructure of thallium-oxide films is quite different than those of In$_2$O$_{3-x}$, In$_x$O, and beryllium. However, strongly-localized films of this material exhibit glassy effects that are essentially identical to those of In$_2$O$_{3-x}$, In$_x$O, and beryllium. These include logarithmic relaxation of the out-of-equilibrium conductance and a memory-dip (MD) that has all the earmarks of intrinsic electron-glass. The width of the memory-dip exhibited by thallium-oxide is observed to be close to that of the electron-rich version of In$_x$O that has similar carrier-concentration. This appears to be in line with a general trend; the MD width of all materials tested so far shows a systematic correlation with carrier-concentration. The possible connection between the memory-dip and the Coulomb-gap, and the origin of similar behavior in granular systems are discussed in light of these findings.

I. INTRODUCTION

The interplay between disorder and interactions in Fermi systems has been a challenging field of research and a source of fascination for more than five decades. A prominent representative of this group, the Anderson transition, has been extensively studied both theoretically and experimentally, and at least qualitatively, its equilibrium properties are well understood. On the other hand, the out-of-equilibrium properties of the insulating phase remains ill-understood and controversial. This applies in particular to the ‘electron-glass’ (EG) scenario discussed in several papers. The EG phase is expected to arise from the competition between disorder and interactions. It is a generic scenario that applies to all degenerate Fermi systems with localized states interacting via a Coulomb potential. It ought to be observed in any strongly-localized system exhibiting hopping transport. Experimental evidence for glassy effects, however, has been somewhat scarce. Intrinsic EG effects were found in several systems but remarkably none was reported in lightly-doped semiconductors. By ‘intrinsic EG’ we mean that the effects appear systematically for a given substance independently of the way the sample was prepared to achieve the same relevant parameters (resistance at the measuring temperature, dimensionality, and carrier-concentration).

It has been conjectured that the reason for the absence of intrinsic EG effects in lightly-doped semiconductors is their inherently short relaxation-time, which makes it hard to resolve these effects by transport measurements. The short relaxation time of semiconductors was alleged to be due to their low carrier-concentrations. This has been supported by a recent experiment on phosphorous-doped silicon where ultra-fast relaxation was found. Conductance relaxations that persist for many seconds, and memory effects characteristic of intrinsic electron-glass, seem to be peculiar to systems with $n>5\times10^{19}$cm$^{-3}$.

II. EXPERIMENTAL

A. Sample preparation and characterization

The Ti$_2$O$_{3-x}$ films used here were e-gun evaporated on room-temperature microscope-slides or, for the field effect measurements, unto the 0.5µm SiO$_2$ layer thermally grown on <100> Si-wafers. The Si wafers were...
boron-doped (P-type) with bulk resistivity $\rho \simeq 2 \times 10^{-3}\Omega\cdot\text{cm}$ deeply into the degenerate regime. They were used in this study as the gate electrode in the field-effect experiments. The substrate was rinsed by ethanol, dried, and was ion-bombarded by O$_2$ in the vacuum chamber prior to material evaporation. The source material was 99% pure Tl$_2$O$_3$ brown powder (American Elements) pressed into the water-cooled copper crucible of the e-gum fixture. Deposition was carried out at (0.5-2)$\times 10^{-4}$ Torr oxygen ambience maintained by leaking 99.9% pure O$_2$ through a needle valve into the vacuum chamber (base pressure $\simeq 10^{-6}$ Torr). Rates of deposition used for the samples reported here were in the range 0.2-4 Å/s monitored in-situ using a quartz thickness-monitor calibrated by a Tolan-sky interferometer.

The Tl$_2$O$_3$ powder temperature during deposition was 600±30K, a much lower evaporation temperature than the ≃1500K used for In$_2$O$_{3-x}$ to obtain similar evaporation rates. Another aspect where Tl$_2$O$_{3-x}$ films differ from In$_2$O$_{3-x}$ films is in the way they respond to different post-preparation treatment. In particular, exposing In$_2$O$_{3-x}$ to UV radiation breaks oxygen bonds, which upon vacuuming are removed from the sample. This in turn increases the carrier-concentration and decreases the sample resistance. The UV treatment is a reversible process by which a given sample resistance may be changed. It works well in In$_2$O$_{3-x}$ films as well as in ZnO crystals, where the resistance may be restored by letting oxygen diffuse back into the sample. Films of Tl$_2$O$_{3-x}$ on the other hand, show no change of resistance when exposed to UV radiation, and are much less susceptible to oxidizing agents than In$_2$O$_{3-x}$. Lacking this flexibility of fine-tuning the disorder, thallium-oxide samples with different resistances have to be made individually. Varying the film thickness in the deposition process was the most effective way to control the sample resistance, and it turned out that small changes around 200Å yielded the range of few kΩ to 100MΩ (at $T$=4K).

Achieving continuous thin-films of this material is a challenging undertaking. This seems to be a problem that plagues other preparation techniques used to produce thin films of this material. This is the reason for the wide range of rates and oxygen pressure mentioned above that were tested in attempting to find the optimal conditions. Variations in the deposition-rates and partial oxygen pressure had much weaker influence on film structure than the type of substrate used; for nominal thickness in the range 200±20 Å the yield of continuous films using (sodium-oxide-rich) microscope-slides was around 80% whereas it was less than 5% (2 in 41 deposition runs) for the SiO$_2$ layer thermally grown on <100> Si-wafers. Much better yield of physically continuous specimen were obtained on both type of substrates by co-depositing Tl$_2$O$_3$ with $\approx$6% Au evaporated from a Knudsen source. The gold deposition rate was adjusted independently from that of the Tl$_2$O$_3$. The Tl$_2$O$_{3-x}$:Au films turned out to be less sensitive to the type of substrate, and they were also more stable against agglomerations and grain-growth than pure films. Grains as large as 2µm could be seen by optical microscopy in Tl$_2$O$_{3-x}$ samples that were heat-treated at $T\geq 450$K. This agglomeration also affected their optical transmission in the visible as shown in Fig. 1 comparing Au-doped with undoped specimen. Susceptibility to agglomeration and the associated grain-growth is the main impediment in getting electrically continuous thin films of the clean material.

Transmission-electron-microscopy (TEM) was used to characterize the films composition and microstructure (employing the Tecnai F20 G2 equipped with an energy dispersive analyzer). Samples studied by TEM were deposited unto carbon-coated Cu grids under the same conditions as those used for transport measurements. TEM micrographs and electron-diffraction patterns of Tl$_2$O$_{3-x}$ and Tl$_2$O$_{3-x}$:Au films are shown in Fig. 2 and Fig. 3 respectively. The main difference between the two types of the Tl$_2$O$_{3-x}$ films is the preponderance of smaller and mid-size grains in the Tl$_2$O$_{3-x}$:Au films, but both show a rather wide distribution of grain-sizes. This should be compared with the space-filling, mosaic structure of In$_2$O$_{3-x}$ films (see e.g., Fig. 1 in [1]).

The diffraction patterns of both types of structures are dominated by the larger grains giving spotty rings which mask the presence of an amorphous component in the as-deposited films. The set of rings could be indexed for 8 of the allowed rings according to the bcc bixbyite structure of the compound with lattice spacing $a\approx 10.53\pm 0.02$Å (see table 1).

Energy-dispersive x-ray spectroscopy revealed about 1% (atomic ) tungsten as the only contaminant on

![FIG. 1: (color online) Optical transmission of 200Å thick Tl$_2$O$_{3-x}$ and Tl$_2$O$_{3-x}$:Au deposited on glass-slide. Full labels - as deposited at room temperatures. Empty labels - after 30 seconds heat-treatment at $T$=490K. Note the large change in transmission for the Tl$_2$O$_{3-x}$ film as compared with the milder effect in the Tl$_2$O$_{3-x}$:Au sample.](image-url)
FIG. 2: Bright-field micrograph of an as-deposited Tl$_2$O$_{3-x}$ film (nominal thickness 200 Å). Note that a typical grain-size rarely exceeds ≃150nm. The inset shows the associated diffraction pattern. Note that the bare areas in the film (white regions in the micrograph) tend to be adjacent to relatively large grains, a consequence of grain growth in a deposit with strong self-affinity. Film continuity involves amorphous (or micro-crystalline phase).

![FIG. 2](image)

FIG. 3: Bright-field micrograph of a typical ≃200Å thick Tl$_2$O$_{3-x}$:Au film. The inset shows the associated diffraction pattern. The magnification is the same as in Fig. 2.

![FIG. 3](image)

TABLE I: Measured vs. calculated d-spacings of the diffraction rings observed in the TEM micrographs

| (hkl) | Observed d (Å) | Calculated d (Å) |
|-------|----------------|------------------|
| (222) | 3.04±0.01      | 3.040            |
| (123) | 2.81±0.01      | 2.814            |
| (400) | 2.64±0.01      | 2.632            |
| (431) | 2.05±0.01      | 2.065            |
| (611) | 1.80±0.01      | 1.806            |
| (622) | 1.59±0.01      | 1.587            |
| (631) | 1.55±0.01      | 1.553            |
| (640) | 1.45±0.01      | 1.460            |

In addition to the rings listed in table 1, Tl$_2$O$_{3-x}$:Au films showed a fcc pattern of Au grains suggesting that most of the material segregated out of the Tl$_2$O$_{3-x}$ matrix. The Au diffraction pattern was used as a guide to calibrate the camera constant. The appearance of free Au particles in the Tl$_2$O$_{3-x}$:Au films is another aspect in which this material differs from In$_2$O$_{3-x}$ based specimen; in the latter system no sign of free Au is observed in the diffraction patterns for similar levels of gold addition, and there are indications that the gold atoms reside in the oxygen vacancies sites.

Samples used for electrical measurements were deposited through rotatable stainless-steel masks to define their geometry and were typically 1x1mm and 200 Å thick. Prior to sample deposition, gold contacts were evaporated through another set of masks on the same fixture which had alignment pins that positioned the contacts on the sample area.

Room temperature Hall-effect measurements were used to determine the carrier-concentration. This was done with three of the batches prepared for the transport measurements using samples with a Hall-bar configuration (six-probe measured by dc). At room temperatures, these films had sheet-resistances $R_{\square}$ of few kΩ making them effectively diffusive, and therefore the Hall-effect may be used as a reliable measurement of the material carrier-concentration. Essentially the same result for the carrier-concentration $n=(1.9\pm0.2)\cdot10^{21}$ cm$^{-3}$ was found for both Tl$_2$O$_{3-x}$ and Tl$_2$O$_{3-x}$:Au films. This value for $n$ is larger by 2-3 than the carrier-concentration found for Tl$_2$O$_{3-x}$ prepared by electrodeposition$^{15}$ and, interestingly, it is almost two orders of magnitude larger than that of In$_2$O$_{3-x}$. No difference in transport properties were found between Tl$_2$O$_{3-x}$ and Tl$_2$O$_{3-x}$:Au films with comparable sheet-resistance $R_{\square}$. It seems that the only role of Au is to curb the tendency of the material to agglomerate.
B. Measurement techniques

Conductivity of the samples was measured using a two-terminal ac technique employing a 1211-ITHACO current pre-amplifier and a PAR-124A lock-in amplifier. Most measurements reported below were performed with the samples immersed in liquid helium at T=4.1K maintained by a 100 liters storage-dewar, which allowed long term measurements of samples as well as a convenient way to maintain a stable temperature bath. Unless otherwise indicated, the ac voltage bias was small enough to ensure linear response conditions (judged by Ohm’s law being obeyed within the experimental error).

The microwaves experiments employed high-power synthesizer (HP8360B) using power up to 25 dBm ($\approx316$ mW) at the frequency range of 2-6 GHz. Optical excitation was accomplished by exposing the sample to AlGaAs diode (operating at $\approx0.88\pm0.05\mu$m), placed $\approx15$mm from the sample. The diode was energized by a computer-controlled Keithley 220 current-source. The samples were attached to a probe equipped with calibrated Ge and Pt thermometers and were wired by triply-shielded cables to BNC connectors at room temperatures. The effective capacitance of the wires was typically 10nF allowing the use of 70-75Hz ac technique in most cases.

Fuller details of measurements techniques are given elsewhere.$^2$

III. RESULTS AND DISCUSSION

A. Hopping conductivity and current-voltage characteristics

We start this section by examining the near-equilibrium (conductance) and steady-state (current-voltage characteristics) properties of the thallium-oxide films with $R_{\parallel} > h/e^2$ (at liquid helium temperature). The only goal in this section is to demonstrate that the $\mathrm{Tl}_2\mathrm{O}_{3-x}$ samples are in the strongly-localized regime, and that their near-equilibrium transport properties cannot be distinguished from those of other hopping systems (including systems that do not exhibit intrinsic electron-glass effects, e.g., lightly-doped semiconductors).

The strongly-localized nature of these films was verified by measuring their conductance versus temperature dependence $G(T)$ at the temperature range 4-45K. Figure 4 illustrates this behavior for two of the samples that were used in this study. Below $\approx10$K, this dependence can be described reasonably well by $G(T) \propto \exp[-(T_0/T)^{1/2}]$ with $x$ either 3 or 4. The limited range of temperature and resistance does not allow distinguishing between these. However, this range is wide enough to exclude $G(T) \propto \exp[-(T_0/T)^{1/2}]$ at least for the sample with the larger resistance in Fig. 4. The form of variable-range-hopping (VRH) shown in Fig. 4 is often observed in strongly-localized $\mathrm{In}_2\mathrm{O}_{3-x}$ samples.$^{16}$ By comparison, over a similar range of temperatures the hopping law $G(T) \propto \exp[-(T_0/T)^{1/2}]$ is obeyed by thin films of beryllium$^{16}$, and by the high-carrier concentration version of $\mathrm{In}_2\mathrm{O}_3$ (with $n \approx 10^{21}$cm$^{-3}$).$^{17}$

One should not take these mathematical fits too seriously. It is actually unclear why these systems should exhibit any specific exponent of VRH: Both, the $\ln(G) \propto T^{-1/3}$ and $\ln(G) \propto T^{-2/3}$ VRH forms are results of models that assume, among other things, single occupation of localized sites. As remarked elsewhere,$^{18}$ this assumption may not justified in systems with carrier-concentration as high as that of $\mathrm{In}_2\mathrm{O}_{3-x}$ (let alone in systems with higher $n$ such as Be and $\mathrm{In}_2\mathrm{O}_3$). In these systems there are many charge-carriers within a localization volume and interactions may modify overlapping electronic states.

There are apparently other factors in hopping conductivity that are not accounted for by existing theories. A pertinent comment on the uncertainty of the hopping exponent in realistic systems was made by Brodsky and Gambino on the basis of their experiments in amorphous Si$^{18}$ (where multi-occupation of localized states is not a concern). Rather, it was the behavior of the pre-exponential factor that led these authors to remark that not much weight should be given even to the value of the exponent when fitting $G(T)$ data. The point is that in reality disordered systems are more complicated than assumed by current theories for hopping conductivity. It is hardly surprising that important deviations from the predictions of hopping models are observed in experiments on real samples. Nonetheless, the exponential temperature dependence of $G$ is a clear indication of the strongly-localized nature of the used films and that is all we need for the main conclusions in this paper.

A characteristic attribute of hopping systems, which further illustrates the inadequacy of current VRH mod-

![FIG. 4: (color online) Temperature dependence of the resistance of two of the films used in the study (one on each of the type of substrates used). The curves are also labeled by their respective activation energy $T_0$. These data may be fitted also by $R(T) \propto \exp[(T_0/T)^{1/2}]$ but not by $R(T) \propto \exp[(T_0/T)^{1/2}]$.](image-url)
FIG. 5: (color online) The dependence of the conductance on the applied voltage for a typical Tl$_2$O$_{3-x}$:Au film (thickness 200 Å, $R_\square=5.7$MΩ, and lateral dimensions 1x1 mm$^2$) measured at $T=4.1$K using phase-sensitive technique at frequency of 74Hz. The inset shows the fractional change of the conductance at the low voltage regime compared with the respective result of using a microwave field at $f=2.45$GHz while measuring G using low frequency Ohmic bias (see text).

els, is their non-Ohmic behavior, which is often observable at lower fields $F$ than anticipated. The common expectation is that Ohmic behavior persists up to fields of order $k_B T/eL$, where $e$ is the electron charge and $L$ is the percolation radius. However, typical values for $L$ determined from the crossover to non-Ohmic behavior often leads to values of $L$ that are much larger than this length scale. The same phenomenon is observed in all our Tl$_2$O$_{3-x}$ and Tl$_2$O$_{3-x}$:Au samples. Figure 5 shows the dependence of the conductance on the applied voltage for a typical Tl$_2$O$_{3-x}$:Au sample.

The inset to Fig. 5 is a zoom-in on the low voltage part of the main G(V) curve taken by a low-frequency ac technique. It is hard to assign a precise value for the voltage above which Ohmic behavior is no longer obeyed in the G(V) curve as the deviation is gradual. A fair estimate based on the data shown in the inset to Fig. 5 would be $V\sim 30$mV where the deviation from Ohmic behavior is well above the experimental error. Using $L\sim b k_B T/e V$ (b is the sample length) gives $L \approx 10$μm, which is much larger than any reasonable estimate for the percolation radius. This problem seems to be the rule in VRH conductivity; similarly large values for $L$ were found by Rosenbaum et al. in doped-Si, and Graman et al. found in Ge samples doped by nuclear transmutation. The possibility that these discrepancies arise from the present of long-range potential fluctuations was discussed in, and experimental evidence for their presence was found in strongly insulating In$_2$O and In$_2$O$_{3-x}$ films.

Finally, the change of the conductance due to application of a microwave field is compared in Fig. 5 (inset) with the G(V) data taken at a low frequency. In the latter case G is still measured at low frequency but as function of the amplitude of a microwave field capacitively coupled to the sample. This microwave enhanced conductivity is another way to modify the hopping conductance and it is essentially a non-Ohmic effect generic to VRH systems. This was shown to exist in several systems including in the lightly-doped GaAs. It was also pointed out that existing models for non-Ohmicity in the VRH regime fail to give a satisfactory fit to the experimental G(V) in these systems.

To sum up this part we conclude that thallium-oxide samples with $R_\square > h/e^2$ (at $T\approx 4$K) exhibit VRH behavior that is similar to other strongly-localized systems including some lightly-doped semiconductors. Their out-of-equilibrium transport features described next, identify them as intrinsic electron-glasses with extended relaxation times as might be expected from their high carrier-concentration on the basis of previous empirical findings. These, as will be discussed below, cannot be accounted for by VRH models that assume single occupation of localized sites.

B. Out of equilibrium transport properties

The first set of experiments, shown in Fig. 6, describes the basic relaxation of the excess conductance following quench-cooling the sample from high temperatures to liquid helium ambience (Fig. 6a). Fig. 6b&c show the results of applying the stress-excitation protocol on the same sample after it was allowed to equilibrate at $T=4.1$K for $\approx 28$ hours. The stress protocol involves subjecting the sample to a large ‘source’-'drain’ field, driving the sample into the non-Ohmic regime, which creates excess phonons and takes the system out of equilibrium. This can be observed during the stress as a slow increase of the conductance (Fig. 6b), and when Ohmic conditions are restored a logarithmic decay of the excess conductance is observed (Fig. 6c).

Another effective way to drive the system far from the equilibrium and observe the ensuing relaxation is by optical excitation. A typical result using this protocol is illustrated in Fig. 7 for a Tl$_2$O$_{3-x}$ film.

Common to the protocols used in Figs. 6 and 7 is that they can be performed on films deposited on any insulating substrate and do not necessitate a gate.

This makes it easier to measure the conductance of a high resistance sample. A nearby metallic gate, a must for the field effect experiments, introduces a parallel capacitance in the measurement circuit and limits the frequency used in the ac technique. Also, comparing the results with Tl$_2$O$_{3-x}$ samples configured with a gate helps to verify that the glassy effects are not due to artifacts associated with trapped charge or other defects in the insulating layer that separates the sample from the gate (this appears to be a problem in some semiconductors). However, as was emphasized elsewhere, the prime sig-
Figure 6: (color online) Two basic manifestations of electron-glass features: Conductance vs. time of a Tl$_2$O$_{3-x}$:Au sample with R$_\square$=5.7MΩ (a): following a quench-cool from T$\approx$110K to T=4.1K. (b): Under the stress of a field F=102V/cm for 1400 seconds, and (c) After the voltage across the sample is set back to an ohmic value.

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As in other electron-glasses, the width Γ of the MD turns out to be independent of R$_\square$ over the range of R$_\square$ between 800kΩ to 30MΩ configured with a gate for field-effect experiments. The MD for the Tl$_2$O$_{3-x}$:Au film tested in a MOSFET configuration is ≈5.7MΩ (same as in §2: Au sample with R$_\square$=11MΩ at T=200kΩ). As can be seen in Fig. 9a, the significance of this observation will be discussed later.

As in other electron-glasses, the width Γ of the MD turns out to be independent of R$_\square$ over the range of 1.1x1.6mm$^2$ (LxW). The gate voltage was swept in this case from $V_g$ = -6.3V to $V_g$ = +6.4V through the $V_g$ = 0V point where the sample was allowed to equilibrate for 31 hours at T=4.1K. The dashed line depicts the slope of the thermodynamic field-effect.

Note that Γ is comparable to that of the electron-rich version of In$_x$O that has a similar value of thickness $3-x$ that was done in §2. Comparing the MD of the Tl$_2$O$_{3-x}$:Au film with R$_\square$=5.7MΩ (same as in Fig. 5&6) with a In$_x$O film with R$_\square$=8.3MΩ. (b) $G(V_g)$ for a diffusive Tl$_2$O$_{3-x}$:Au sample (thickness 220Å, R$_\square$=4.1kΩ).

The presence of a memory-dip in the $G(V_g)$ scans is only observable at T=4K for samples with R$_\square$ > 200kΩ. Figure 9b shows, on the same gate-voltage scale, the

FIG. 7: (color online) Typical result of an optical excitation protocol using a Tl$_2$O$_{3-x}$:Au sample with R$_\square$=11MΩ at T=4.1K. Following a 3s exposure to infrared light (LED energized by 50mA at 1.5 cm from sample), the conductance shows the characteristic logarithmic relaxation law as illustrated in the inset.

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FIG. 8: (color online) The MD for a Tl$_2$O$_{3-x}$:Au sample with R$_\square$=43.9MΩ, thickness≈195Å and lateral dimensions of 1.1x1.6mm$^2$ (LxW). The gate voltage was swept in this case from $V_g$ = -6.3V to $V_g$ = +6.4V through the $V_g$ = 0V point where the sample was allowed to equilibrate for 31 hours at T=4.1K. The dashed line depicts the slope of the thermodynamic field-effect.
field effect taken with another FET-like structure on a Ti$_2$O$_{3-x}$:Au film with a lower disorder. This sample had $R_\square<h/2\pi$ and, at this temperature in the diffusive regime which, as might be expected, shows no sign of a MD. Rather, the $G(V_g)$ curve in Fig. 9b exhibits only the thermodynamic field-effect produced by a slightly concave $G(V_g)$ curve presumably reflecting the energy dependence of the density of states $\frac{\partial}{\partial\mu}(\varepsilon)$. The curvature of this curve is typical to a disorder-modified $\frac{\partial}{\partial\mu}(\varepsilon)$ at the tail of the conduction band (note that the Fermi energy associated with $n\approx10^{21}\text{cm}^{-3}$ is near the bottom of the band). The $\partial G/\partial V_g>0$ is consistent with the material being n-type degenerate semiconductor.$^{18}$

The thermodynamic contribution to the field-effect is observable whether the system is glassy or not. For samples in the glassy regime it appears as an anti-symmetric component in $\partial G/\partial V_g$. Another way to see the relative contributions of the non-equilibrium and thermodynamic components is in the temporal response of the conductance to a one-step change in $V_g$. An example of such a protocol is illustrated in Fig. 10. This is another method of driving the system out of equilibrium and observe the ensuing relaxation.

There are two fundamental properties that the memory-dip exhibits. First, its position on the gate-voltage scale, that in the above plots is centered at $V_g=0$, depends on the gate-voltage at which the system was allowed to equilibrate. Secondly, it has a characteristic shape that does not depend on whether it was recorded by starting the sweep away from the equilibrium $V_g$ towards either polarity or by sweeping $V_g$ through the equilibrium point. These two features, previously studied in the In$_3$O$_{3-x}$ and In$_x$O samples,$^2$, are illustrated in Fig. 11.

The figure shows a set of recorded events where initially the sample was cooled and equilibrated while holding the gate-voltage at $V_g=-4.6V$. After equilibration, the two different sweep protocols were taken to show that the MD is now centered at $+2.6V$, and that the shape of the MD is essentially the same for both protocols. Then, $V_g$ was moved to $V_g=0V$ and it was held there for 24 hours. Subsequent scans of $V_g$ now reveal the MD centered at the new equilibration position while the old MD has almost vanished (leaving a small bulge at the right-wing of the ‘new’ MD).

The non-equilibrium transport features described above are remarkably similar to those reported in other intrinsic electron-glasses in all aspects and, in particular, in the phenomenology associated with the MD. To see how the width of the MD fits the dependence on carrier-concentration we give in Fig. 12 the width $\Gamma$ of other non-granular electron-glasses measured to date. In the figure $\Gamma$ is given in energy units calculated from the experimentally measured width $\delta V_g^{(1/2)}$ (see e.g., Fig. 9a) by: $\Gamma = \frac{\delta V_g^{(1/2)} C}{\frac{\partial n}{\partial \mu}(\varepsilon_F)}$. Here $C$ is the sample-to-gate capacitance (per unit area), $\frac{\partial n}{\partial \mu}(\varepsilon_F)$ the material DOS at the Fermi energy, $\varepsilon_F$ is the electron-charges, and $\lambda$ is the screening-length. $\frac{\partial n}{\partial \mu}(\varepsilon_F)$ and $\lambda$ were estimated from the material carrier-concentration $n$ using free-electron formulae. The values of $\Gamma$ obtained in this way are shown in figure 12 as a function of the inter-carrier distance $<r>\propto n^{-1/3}$. The carrier-concentration is based on Hall effect measurement performed for each sample included in the figure. The single data point for In$_3$O$_{3-x}$ is actually the averaged value for 24 measured samples. Similarly, the data for beryllium is the average of 9 samples.$^{12}$, the
data for In$_2$O$_{3-x}$:Au is based on 5 samples, and the data for Tl$_2$O$_{3-x}$:Au is based on the 5 samples of the present study. Amorphous indium-oxide, In$_2$O, is the only EG material studied to date where a study of samples over a wide range of $n$ has been achievable. However, all the other systems follow the same systematic dependence on $n$ as the In$_2$O samples.

It is noteworthy that every granular metal that has been tested show electron-glass effects that are quite similar to those of the Anderson insulators in Fig. 12. The studied granular materials include granular-Pl$_{32}$, granular-AI$_{27}$, and discontinuous films of Au$_{28}$, Ni and Ag$_{42}$. In the hopping regime, all these systems exhibit a memory-dip with $\Gamma$ values that are at the high end of the group depicted in Fig. 12. These are not shown in the figure because their carrier-concentration was not measured. Nonetheless, it is plausible that $n$ in such systems is on the high side, which lends further support to the correlation between carrier-concentration and $\Gamma$.

In an earlier work where $\Gamma(n)$ was studied (Fig. 4 in 8), the possible connection between the MD and the Coulomb-gap was considered. Some of the reservations raised in 8 with this line of interpretation were later relaxed 9. The correlation between $\Gamma$, that by now has been fortified by adding more samples and three more Anderson insulators, is suggestive of a generic mechanism. This lead us to re-examine the connection between the Coulomb-gap and the memory-dip.

The Coulomb gap (CG), first discussed by Pollak 30 and Srinivasan 31, is a consequence of the loss of screening in the disordered medium, which makes the interaction long-ranged. Efros and Shklovskii has shown how this leads to a soft gap in the single-particle DOS of the system. There are two features of the CG that are reminiscent of the memory-dip main characteristics. First, the CG is a depression in the single particle density of states $N(\varepsilon)$ with its minimum pinned to the Fermi energy $\varepsilon_F$. This would be a natural explanation for the observation that the MD is centered at the gate-voltage at which the system equilibrated as well as for the two-dip-experiment (Fig. 11 above 33 and references therein). Second, the correlation between the MD width and carrier-concentration (Fig. 7) is also in accord with the CG scenario; it is expected that the energy scale due to interactions will be larger in systems with higher carrier-concentration.

The possible relevance of the Coulomb-gap to the non-equilibrium features observed in the intrinsic electron-glasses was considered by Clare Yu 34 and by Lebanon and Müller 32,33. Yu has adopted the Efros-Shklovskii approach according to which the Coulomb-gap determines the system conductance. This allowed her to reproduce the evolution with time of the MD following a quench from high temperatures. Lebanon and Müller, based on similar ideas, developed a model that accounts for many of the observed electron-glass features. In particular, they gave a plausible interpretation to the temperature dependence of the MD shape 32. This is one of the features that distinguishes the MD of the electron-glass from the cusp that appears in the structural two-level-system 36,37: the shape of the cusp in the structural two-level system does not change with temperature whereas the MD shape is very sensitive to temperature 33.

The consistency of the theoretical approaches 32–35 with the main features of the experiments is encouraging. It does look as a step in the right direction. At the same time, there are questions of fundamental nature that should be addressed. The first question is the subtle issue of the connection between a single-particle DOS and any equilibrium (or near equilibrium) quantity like conductivity. Patrick Lee has commented on this issue with regard to the Thomas-Fermi screening length and the use of the Einstein relation 38. He pointed out that in both cases it is the thermodynamic DOS $\partial n/\partial \mu$ that is the relevant quantity.

The single-particle DOS is relevant for processes associated with insertion (removal) of a particle into (from) the system while no relaxation of other particles takes place, which would be the case in tunneling or photoemission events. By contrast, the field effect is usually conceived in the same category as conductance in this respect.

In the current situation we are in an uncharted territory; the process of sweeping the gate voltage involves inserting (removing) particles while "some fast things have happened but some slow things have not", which means: things are changing even as we sweep. Under these nonequilibrium conditions it is not clear whether the use of the Einstein relation is justified. One may argue that if the sweep duration is short relative to the relaxation time (yet keeping $\Delta V_g/\Delta t$ small enough to minimize the risk of structural changes that may be caused...
by the sweep), the situation is no different than the near-equilibrium conditions encountered in real-life situations. There are no indication from our non-equilibrium field-effect experiments to contradict this point of view. In fact, the dependence of the MD magnitude on the gate-voltage scan-rate seems to be consistent with it; it is found (Fig. 4 in) that the MD magnitude increases with the scan-rate with the same logarithmic law that controls the time-relaxation of the excess conductance. It may be said that \( G(V_g) \) is a snap-shot of a DOS made observable by a scan that occurred while some particles in the system are effectively frozen. Whether these crude ideas are justified or not must await a proper theory for field-effect experiments in out-of-equilibrium situations.

Even if it is the single-particle DOS that modulates \( G(V_g) \), it is not clear what functional form should be taken for it. The problem is not only the multiplicity of forms derived for the Coulomb gap by different authors\(^{35,39-44}\); it is rather the basic model used; essentially all Coulomb-gap models assume single-occupation of sites while the one features common to all systems that exhibit MD is that their localized states contain many particles even for strong disorder. There were several attempts to include quantum effects to assess their modifications to the Coulomb gap\(^{30,41,45-50}\). There were also some attempts to consider double-occupation of the localized states that already introduced new effects that are manifest in magneto-conductance measurements\(^{31}\). However, to our knowledge, no treatment of the Coulomb gap for the multi-occupation scenario has been attempted.

The observation that a memory-dip is seen only in electronic systems containing many particles in a localization volume even when strongly localized\(^{52}\) may be an important clue to the dynamics of the electron-glass. Multiply-populated localized-sites are essentially small (disordered) metals. Tunneling transitions between these mesoscopic elements would induce a many-body shake-up process which may reduce transition probabilities due to the Anderson orthogonality-catastrophe (AOC)\(^{53}\). While this is probably a small effect for transport, it may be significant factor in determining the relaxation rate. The space-energy charge organization, building up the Coulomb-gap from the out of equilibrium random distribution, involves many more sites than those participating in the transport. Moreover, many-sites simultaneous transitions are required to approach the lowest energy configuration, while transport is essentially a single-particle process. The necessity of many-particle transitions for achieving the ground state was realized by Baranovski et al in computer simulations\(^{54}\).

In sum, we presented data on the structure and transport properties of thallium-oxide films. In the Anderson insulating regime these films exhibit hopping conductivity and current-voltage characteristics that are commonly found in other insulating systems at low temperatures. Their non-equilibrium transport features are in line with those previously reported in other electron-glasses. In particular, they exhibit a memory-dip that is characterized by an energy width that fits the empirical relation relating the width to the carrier-concentration of the material. This feature makes it a challenge to account for the memory-dip by a mechanism that links the glassy effects with 1/f noise\(^{55}\).

A common feature shared by all the systems that exhibit intrinsic electron-glass behavior is high carrier-concentration. This presumably is what distinguishes them from the lightly-doped semiconductors. Near the transition to the diffusive regime (or when the dielectric constant of the medium is very large), the electron-electron interaction will be much smaller than the disorder and therefore the element of frustration, crucial for glassy behavior, may not be fulfilled. Both strong disorder and comparably strong interactions are presumably needed for the glassy phase.

Empirically, Anderson insulators with higher carrier-concentration tend to exhibit long relaxation times. Granular metals present a special case of strongly-localized systems with high carrier-concentration and it is remarkable that they systematically exhibit MD and long relaxation times. Note that the other feature they share with the systems in Fig. 12 is many electrons per ‘localization volume’. The empirical evidence in favor of the conjecture that multi-occupation is the reason for the long relaxation times is compelling enough to warrant a serious theoretical effort to explore the possibility that many-body effects are involved.

To further test the empirical connection between carrier concentration and relaxation time, it is desirable to include more materials in the experimental study. Both low and high carrier-concentration should be tested. On the theoretical side, there is the challenge of dealing with the consequences to hopping transport due to multi-occupation of electronic states, and the connection between the single-particle DOS and conductivity in non-equilibrium situations.

Acknowledgement 1 I am indebted to Dr. Tsirlina for drawing my attention to the special qualities of thallium-oxide and for sharing her experience in sample preparation. This research has been supported by a grant administered by the Israel Academy for Sciences and Humanities.

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