Abstract. We investigate the implications of a massive binary system in the centre of the gamma-ray blazar Mkn 501 and show that the periodical behaviour recently observed in the TeV and X-ray lightcurves may possibly be related to the orbital motion of the relativistic jet emerging from the less massive black hole. For the special relativistic jet properties inferred from emission models, we derive an intrinsic orbital period of \((6 - 14)\) yrs and a centre-of-mass distance of \((2.0 - 3.5) \times 10^{16}\) cm. If the binary is very close with a separation of the order of that for which gravitational radiation becomes dominant, we find a maximum primary mass of \(\sim 10^8 M_\odot\) and a corresponding secondary mass in the range of \(\sim (4 - 42) \times 10^6 M_\odot\) depending on the intrinsic jet properties. Such values are in line with the black hole masses expected from merger scenarios.

Key words: Galaxies: active – BL Lacertae objects: individual: Mkn 501 – Galaxies: jets

1. Introduction

Binary black hole systems (BBHSs) are expected to be common in the universe as a result of mergers between galaxies. In the underlying picture for the morphological evolution, galaxies were formed as part of a hierarchical clustering process (e.g. White 1997). Giant elliptical galaxies, such as the host galaxy of Mkn 501, appear to be the products of mergers between spiral galaxies (cf. Fritz v.-Alvensleben 1996). Since the brightest galaxies generally seem to contain massive black holes in their nuclei (e.g. Rees 1984; Kormendy & Richstone 1995; Ho 1998; Magorrian et al. 1998; Richstone et al. 1998), merging would naturally lead to the formation of massive BBHS (Begelman et al. 1980, abbreviated: BBR 80; Rees 1994; Artymowicz 1998; Richstone 1998). The so formed binary black hole is expected to spend most of its time at a separation of \(\sim 0.1 - 1\) pc for masses of \(10^8 M_\odot\) (BBR 80). However if the binary looses further angular momentum e.g. by slingshot interaction with new stars from subsequent merging events (Roos 1988; Roos et al. 1993), infall of gas (BBR 80; cf. also Gould & Rix 2000) or by interactions with an accretion disk (Ivanov et al. 1999), gravitational radiation will eventually become important and the binary evolution could proceed rapidly to coalescence.

Up to now, several phenomena have been attributed to BBHSs: e.g. misalignment (cf. Conway & Wrobel 1995), precession (BBR 80) or wiggling of jets, where the latter is supposed to be induced by the orbital motion (Kaastra & Roos 1992; Roos et al. 1993). Periodic outburst activity in the quasar OJ 287, has commonly been related to a BBHS and is thought to arise due to tidal perturbation (Sillanpää et al. 1988) or due to one black hole crossing the accretion disk of the other (Letho & Valtonen 1996). Other BBHS scenarios assume a pair of bent jets (Villata et al. 1998) or the precession of the disk under the gravitational torque (Katz 1997).

In the particular case of Mkn 501, the complex morphology of its radio jet and the peculiar behaviour of its spectral energy distribution (SED) have prompted elaborate models relating these properties to a BBHS: Conway & Wrobel (1995), for example, have proposed a saturated helix model in order to explain the misalignment of the radio jet on parsec and kiloparsec scales. Villata & Bai (1999) have argued that the X-ray variations in the SED of Mkn 501 might be due solely to the changing orientation of a helical synchrotron emitting jet in a close BBHS. The recent discovery of periodicity in the TeV and X-ray fluxes believed to be associated with moving features in the jet of Mkn 501 might add another aspect for assessing the relevance of a BBHS in this galaxy.

Mkn 501 is one of at least four active galactic nuclei which have been detected at TeV energies (for review, see Catanese & Weekes 1999). Being the second closest among these with a redshift of \(z = 0.034\), Mkn 501 has been historically classified as an X-ray selected BL Lac object showing virtually no emission lines, and is hosted by the elliptical galaxy UGC 10599 (Stickel at al. 1993). As a BL Lac object, Mkn 501 belongs to the blazar class of AGN which are thought to have relativistic jets oriented...
at a small viewing angle, thus yielding a strong Doppler enhancement of the observed flux.

At the beginning of 1997, Mkn 501 had suddenly undergone a phase of high activity becoming the brightest source in the sky at TeV energies. Subsequent multiwavelength campaigns revealed a variable, two component SED with a low energy part extending up to 100 keV (Pian et al. 1998) and a high energy part which extends at least up to 20 TeV (Samuelson et al. 1998; Konopelko 1999). During this activity phase, particular types of variability have been observed (e.g. Protheroe et al. 1998), consisting of flaring episodes of several days and additional intraday-variabilities. While the TeV and X-rays variations seem to be well correlated, the evidence for correlations with the optical U-band appears to be rather weak (e.g. Catanese et al. 1997; Djannati-Atai et al. 1999; Aharonian et al. 1999).

One of the most fascinating features is the observed periodicity in the flaring state which propagates outwards from the core along the jet by a relativistic emission region (e.g. knot, blob, shock) X-ray and by the less massive black hole and that the nonthermal stant.

**G**

larger hole, respectively, and

\[ S(t) = \delta(t) S'(t') = \delta^{3+\alpha} S'(t'), \]  

(2)

where \( S' \) is the spectral flux density measured in the co-moving frame, \( \delta(t) = 1/(\gamma_b [1 - \beta_b \cos \theta(t)]) \) the Doppler factor, \( \theta(t) \) is the actual angle between the velocity \( \beta_b = \dot{x}_b(t)/c \) of the emission region and the direction of the observer, and where the final equality holds if the source has a spectral index \( \alpha \).

Due to the orbital motion around the center-of-mass, the Doppler factor for the emission region is a periodic function of time. In the simplest case where the angle between the jet axis and the direction of the total angular momentum of the binary is assumed to be zero (e.g. neglecting any kind of precessional motion) the Doppler factor may be written as

\[ \delta = \frac{\sqrt{1 - (v_z^2 + \Omega_k^2 R^2)/c^2}}{1 - (v_z \cos i - \Omega_k R \sin i \sin \Omega_k t)/c}, \]  

(3)

with \( R = M d/(m + M) \) being the centre-of-mass distance, \( v_z \) the outflow velocity in the direction of the total angular momentum, \( i \) the inclination between the jet axis and the line of sight and \( c \) the velocity of light. Obviously, the Doppler factor becomes maximal for \( t = 0.75 P_k \) and minimal for \( t = 0.25 P_k \), where \( P_k = 2 \pi/\Omega_k \) denotes the keplerian period.

From the TeV flux ratio of \( f \sim 8 \) between the maximum and the minimum state during the observation (cf. Protheroe et al. 1998; Hayashida et al. 1998, Aharonian et al. 1999) and the assumption that the periodicity arise in the main due to geometrical origin, we now obtain the condition \( \delta_{\text{max}}/\delta_{\text{min}} \approx f^{1/(3+\alpha)} \) (see Eq. (2)). Consequently, by using Eq. (3) one finds

\[ \Omega_k R = \frac{f^{1/(3+\alpha)} - 1}{f^{1/(3+\alpha)} + 1} \left( \frac{1}{\sin i} - \frac{v_z}{c} \cot i \right) c. \]  

(4)

For a source region which moves in the time interval \( dt \) from point \( A \) to point \( B \) with relativistic velocity \( v_z \) and at an angle \( \psi \) to the line of sight, the observed difference in arrival times for radiation emitted at \( A \) and \( B \) is generally given by \( d t_{\text{obs}} = d t - d t (v_z/c) \cos \psi \), thus leading to a shortening of the observed time interval. Along this line of argument, one may easily derive that the observer in the model presented here will only perceive a strongly shortened period, i.e. the observed period \( P_{\text{obs}} \) is related to the intrinsic period \( P_k \) by (cf. also Camenzind & Krokenberger 1992, Roland et al. 1994)

\[ P_{\text{obs}} = (1 + z) \int_0^{P_k} (1 - \beta_b \cos \theta(t)) \, dt. \]  

(5)
Performing the integration, one immediately arrives at

\[ P_{\text{obs}} = (1 + z) \left( 1 - \frac{v_z}{c} \cos i \right) P_k. \] (6)

From the theoretical point of view, relativistic blazar jets are thought to be oriented at a small viewing angle. Current emission models favour an inclination angle \( i \simeq 1/\gamma_b \) (Spada 1999; cf. also Chiaberge et al. 2000) with typical bulk Lorentz factors in the range 10 – 15 (e.g. Mannheim et al. 1996; Hillas 1999; Spada et al. 1999). For such values and by using an observed period of 23 days and a characteristic outflow velocity of \( v_z/c \approx (1 - 1/\gamma_b^2)^{0.5} \), Eq. (5) results in an intrinsic period of \( P_k = (6 - 14) \) yrs.

Combining Eq. (5) and Eq. (6) we may also derive an expression for the the centre-of-mass distance

\[ R = \frac{P_{\text{obs}}}{2 \pi (1 + z) ^{(f + i/3)} - 1} \frac{c}{f^{1/(3+\alpha) + 1} \sin i}. \] (7)

Given the observed period and the spectral index, Eq. (6) only depends on the inclination angle. Accordingly, for an observed period of 23 days, a ratio \( f = 8 \) and a TeV spectral index of \( \alpha \simeq 1.2 \) (Aharonian et al. 1999), one gets \( R \approx (2.0 - 3.5) \times 10^{16} \) cm using the inclination values above.

By inserting Eq. (3) in Eq. (7), the appropriate binary mass ratio is given by

\[ \frac{M}{(m + M)^2/3} = \frac{P_{\text{obs}}^{1/3}}{(2 \pi [1 + z] G)^{1/3}} \frac{c}{\sin i} \times f^{1/(3+\alpha) - 1} \left( 1 - \frac{v_z}{c} \cos i \right)^{2/3}. \] (8)

For a secondary mass in the range of \((10^6 - 10^8) M_\odot\) the required primary masses are calculated in Fig. 3 (see the curves \( K(10), K(15) \)) for two different inclination angles and \( f = 8 \) yielding primary masses of the order of \( 10^8 M_\odot \).

### 2.2. A gravitational constraint on the binary separation

Observationally, BL Lacs are in general less luminous radio sources, showing a lack of strong optical emission lines and little signs of cosmological evolution (cf. Bade et al. 1998; Cavaliere & Malquori 1999). Celotti et al. (1998) have suggested that BL Lac objects correspond to the final evolutionary stage of sources accreting at low radiative efficiencies (i.e. a dormant black hole system), which seems to be supported by HST observation indicating that the less luminous AGN stages occur after the original quasar has dimmed (Bahcall et al. 1994). Recently, Villata & Raiteri (1999) have argued that BL Lacs represent advanced and close BBHS with a decreased mass accretion rate, the binary separation in the case of Mkn 501 being of the order of that for which gravitational radiation becomes dominant. Thus, we might set an upper limit on the allowed binary masses in Mkn 501 by assuming that the current separation equals the gravitational separation \( d_g \), i.e. the position where the gas dynamical time scale is balanced by the time scale for gravitational energy losses (BBR 80). Gas, which may be constantly supplied for example by tidal interaction between galaxies (cf. Heidt 1999) and accreted onto the more massive black hole, will cause the binary separation to shrink on a time scale \( t_{\text{gas}} \approx M (1 M_\odot \text{yr}^{-1}/M) \), with \( M \) the accretion rate (BBR 80). For a simple estimate let us assume that during the optical bright QSO phase mass accretion occurs at about the Eddington limit. The phase of nuclear activity seems to be rather short with a typical duration of a few times \( 10^7 \) yrs (Haehnelt et al. 1998; Richstone et al. 1998). In particular, for a duration of nuclear activity of the order of the salpeter lifetime \( t_s = cc_T c/4 \pi G m_p = 4.5 \times 10^8 \) yrs and for a primary black hole mass of \( \sim 10^8 M_\odot \), gas infall rates of \( \sim 2 M_\odot \text{yr}^{-1} \) are required to sustain the Eddington luminosity, using a canonical 10% efficiency. On the other hand, assuming a circular orbit, the time scale for gravitational radiation is given by \( t_{\text{grav}} = 6.3 \times 10^4 d_{10}^4/(m_8 m_8 [m_8 + m_8]) \) yrs, where the distance and the masses are expressed in units of \( 10^{16} \) cm and \( 10^8 M_\odot \), respectively. Thus, by equating the gas dynamical time scale \( t_{\text{gas}} \) with \( t_{\text{grav}} \), the separation at which gravitational radiation becomes dominant may be written as

\[ d_{g_{\alpha}} = 6.3 M_8^{1/2} m_8^{1/4} (m_8 + m_8)^{1/4} \left( \frac{M_{\odot} \text{yr}^{-1}}{M} \right)^{1/4}. \] (9)

From Eq. (5) and Eq. (6) we immediately get the relation

\[ \frac{M^{1/2} m^{1/4}}{(m + M)^{1/12}} = 1.29 \times 10^{22} \left( \frac{M}{M_{\odot} \text{yr}^{-1}} \right)^{1/4} \times \frac{P_{\text{obs}}^{3/2}}{(2 \pi [1 + z] G)^{1/3}} \left( 1 - \frac{v_z}{c} \cos i \right)^{2/3}. \] (10)

This mass dependence is illustrated in Fig. 4 (curves G). The respective upper limit is given by the point of intersection with the relevant curve \( K \). For example, applying \( \alpha = 1.2 \) and using \( i = 1/10 \), we have a maximum secondary mass \( m \approx 4 \times 10^8 M_\odot \) and a corresponding primary mass of \( M \approx 10^8 M_\odot \) (cf. also Table 1). The masses shown in Fig. 4 are in a reasonable range for ellipticals. Masses of the order of one million solar masses for the companion black hole appear to be in agreement with the concept that the galaxy swallowed in the merger process was a minor spiral galaxy. On the other hand, the host galaxy of Mkn 501 seems to belong to these classes of ellipticals which have black holes in the centers of at least a few hundred million solar masses. Therefore, the binary scenario for Mkn 501 seems not unlikely.

### 3. Discussion

In this paper we have suggested that the periodicity in the flaring state observed in Mkn 501 might be caused
by the orbital motion of the jet in a close BBHS. Applying a simple toy-model we have shown that the BBHS may have a period of $\sim (6 - 14)$ yrs and a centre-of-mass distance of $\sim (2.0 - 3.5) \times 10^{16}$ cm. If one assumes that this separation corresponds to the distance at which gravitational radiation becomes important, several upper limits for the binary masses may be derived. These mass ranges, which are shown in Table 1 using an observed period $P_{\text{obs}} = 23$ days seem to be in line with the expectations from merger scenarios and the suggestions made by Villata & Raiteri (1999).

The TeV observations indicate that we may have $N \leq 6$ for the number $N$ of periodic oscillations (cf. Aharonian et al. 1999; Catanese & Weekes 1999; Quinn et al. 1999), which results in a required propagation length for the emitting component of $l_\gamma = N P_k v_\gamma \simeq 11 - 26$ pc. Thus, for the projected length at the position of Mkn 501 one finds $l_p \simeq 1.4 - 2.1$ mas for $i = (1/15) - (1/10)$ rad. Remarkably, the jet of Mkn 501 bends dramatically at about 3 mas from the core (Marscher 1999). Hence, a change in the jet parameters might be the reason for the termination of the observed periodicity.

For the proposed model to be valid, the jet has to be perfectly collimated with an intrinsic opening angle of less then $\arctan(d/l_\gamma) \sim 0.05^\circ$. Such values are indeed expected in scenarios for the formation and collimation of magnetized BL Lac jets (cf. Camenzind & Krockenberger 1992; Appl & Camenzind 1993; Schramm et al. 1993). At first sight, such a cylindrical jet structure seems to be at least $\sim 20$ times more collimated than the jet seen on VLBA maps (cf. Marscher 1999). However, there is evidence for an at least two-component jet structure in Mkn 501 suggesting an inner spine with transverse magnetic field and an envelope with longitudinal magnetic field (Aaron 1999; Marscher 1999), the polarization properties of the inner spine strongly supporting shocked-jet models (cf. Attridge et al. 1999). In fact, our model requires that the high energy emission originates in a channel along the jet axis as in two-fluid models (e.g. Sol et al. 1989, Roland et al. 1994), the inner emission probably being self-absorbed on the VLBA scale. Recent observations of radio jets indeed indicate a confinement of the higher energy emission to a well-defined channel within a much more extended radio emission (Bahcall et al. 1995; Perlman et al. 1999; Swain et al. 1999). The unification of BL Lacs and FR I objects may add another piece of evidence to such a jet configuration: in order to account for the observed spectral properties an at least two-fold jet velocity structure seems to be required in which a fast spine is surrounded by a slow (but still relativistic) layer (Chiaberge et al. 2000). Support for such a possibility is positively provided by numerical simulations (cf. Aloy et al. 2000; Frank et al. 2000).

For a TeV flux ratio between minimum and maximum of $\sim 8$, the corresponding shift in the break frequency would be given by a factor of $\sim (1.5 - 1.6)$ while the X-ray flux ratio becomes $\sim (5 - 7)$ applying an hard X-ray spectral index $\alpha \simeq 0.6 - 0.9$ (cf. Lamer & Wagner 1998; Pian et al. 1998). Such values seem to be consistent with BeppoSAX observations (Pian et al. 1998) and may also be recovered, using a broken power law fit, in RXTE observations of Mkn 501 (cf. Krawczynski et al. 2000, their Figs.1 and 2a). Gamma-ray observations carried out by the CAT Telescope also reveal a shift of the maximum peak energy apparently in accordance with the expectation above (Djannati-Atai et al. 1999). Small changes in the maxi-

---

**Table 1.** Maximum binary masses, separation $d$, intrinsic orbital period $P_k$, gravitational lifetime $\tau_{grav}$ and precessional period $P_p$ for inclination angles $i$, accretion rate $\dot{M} = 2 M_\odot/yr$ and spectral index $\alpha = 1.2$ (1.7).
mum electron Lorentz factor or the magnetic field along the trajectory of the emission region may further add to flux variations. If there is indeed an additional flux contribution, e.g. low energy emission from the layer, a stationary component comparable to the observed infrared-optical flux (e.g. Pian et al. 1998; cf. also Kataoka et al. 1999) or an additional component responsible for the soft X-ray emission (e.g. Lamer & Wagner 1998; Wagner et al. 1999), the amplitude of the Doppler modulation may decrease to lower frequencies.

In the simple model presented above, we have not yet considered the influence of jet precession due to gravitomagnetic and geodetic origin with a period \( P_b \simeq 580 \times \varepsilon_{16}^{3/2} (M_8 + m_8)^{1/2} m_8^{-1} M_8^{-1} (1+3M/4m)^{-1}\) yrs (cf. Thorne et al. 1986). Since this driving period is much larger than the orbital period (cf. Table 1), a precessional modulation should be negligible during a few revolutions. Interestingly, a precessional period of \( 10^8 \) yrs agrees with the driving frequency found by Conway & Wrobel (1995) in order to explain the misalignment of the radio jet in Mkn 501 on parsec and kiloparsec scale (see also Villata & Raiteri 1999). If the binary hypothesis is correct, the observable period should remain similar during different outburst phases unless there is a change in the general jet properties. For example, an increase in the observed period should then be accompanied by a decrease in the bulk Lorentz factor or, on larger time scales, by an increase of the inclination angle due to the jet precession (cf. also Eq. 5).

Acknowledgements. We would like to thank an anonymous referee for useful suggestions. K.M. acknowledges support from a Heisenberg-Fellowship and F.M.R. from DFG Ma 1545/2-1.

References

Aaron S.E., 1999, in: Takalo L.O., Sillanpää A. (eds.), BL Lac Phenomenon. PASP Conf. Ser. 159, p. 427
Aharonian F., Akhperjanian A.G., Barrio J.A., et al. 1999, A&A 349, 29
Aloy M.-A., Gómez J.-L., Ibáñez J.-M., et al. 2000, ApJ 532, L85
Appi S., Camenzind M., 1993, A&A 270, 71
Artymowicz P., 1998, in: Abramowicz M.A. et al. (eds.), Theory of Black Hole Accretion Disks, Cambridge: Univ. Press, p. 202
Attridge J.M., Roberts D.H., Wardle J.F.C., 1999, ApJ 518, L87
Bade N., Beckmann V., Douglas N.G., et al. 1998, A&A 334, 459
Bahcall J.N., Kirhakos S., Schneider D.P., 1994, ApJ 435, L11
Bahcall J.N., Kirhakos S., Schneider D.P., et al. 1995, ApJ 452, L91
Begelman M.C., Blandford R.D., Rees M.J., 1980, Nat 287, 307. (BBR 80)
Camenzind M., Krockenberger M., 1992, A&A 255, 59
Catanese M., Weekes T.C., 1999, PASP 111, 1193
Catanese M., Bradbury S.M., Bresolin A.C., et al. 1997, ApJ 487, L143
Cavaliere A., Malquori D., 1999, ApJ 516, L9
Celotti A., Fabian A.C., Rees M.J., 1998, MNRAS 293, 239
Chiaberge M., Celotti A., Capetti A., Ghisellini G., 2000, A&A 358, 104
Conway J.E., Wrobel J.M., 1995, ApJ 439, 98
Djannati-Atai A., Piron F., Barrau A., et al. 1999, A&A 350, 17
Frank A., Lery T., Gardiner T.A., et al. 2000, ApJ, in press
Fritze v.-Alvensleben U., 1996, in: Leitherer C. et al. (eds), From Stars to Galaxies, ASP Conf. Ser. 98, p. 496
Gould A., Rix, H.-W., 2000, ApJ 532, L29
Haehnelt M.G., Natarajan P., Rees M., 1998, MNRAS 300, 81
Hayashida N., Hiraiwa H., Ishikawa F., et al. 1998, ApJ 504, L71
Heidt J., 1999, in: Takalo L.O., Sillanpää A. (eds.), BL Lac Phenomenon, PASP Conf. Ser. 159, p. 367
Hillas A.M., 1999, Astropart. Phys. 11, 27
Ho L.C., 1998, in: Chakrabarti S.K. (ed.), Observational Evidence for Black Holes in the Universe. Dordrecht: Kluwer, p. 157
Ivanov P.B., Papaloizou J.C.B., Polnarev A.G., 1999, MNRAS 307, 79
Kaastra J.S., Roos N., 1992, A&A 254, 96
Kataoka J., Mattox J.R., Quinn J., et al. 1999, ApJ 514, 138
Katz J.I., 1997, ApJ 478, 527
Konopelko A., 1999, Astropart. Phys. 11, 135
Kormendy J., Richstone D., 1995, ARA&A 33, 581
Krichen D., deJager O.C., Kestel M., et al. 1999, in: Proc. of 26th International Cosmic Ray Conference (Salt Lake City) 3, p. 358
Krawczynski H., Coppi, P.S., Maccarone T., Aharonian F.A., 2000, A&A 353, 97
Lamer G., Wagner S.J., 1998, A&A 331, L13
Letho H.J., Valtonen M.J., 1996, ApJ 460, 207
Magorrian J., Tremaine S., Richstone D., et al. 1998, AJ 115, 2285
Mannheim K., Westerhoff S., Meyer H., Fink H.-H., 1996, A&A 315, 77
Marscher A.P., 1999, Astropart. Phys. 11, 19
Nishikawa D., Hayashi S., Chamoto N., et al. 1999, in: Proc. of 26th International Cosmic Ray Conference (Salt Lake City) 3, p. 354
Perlman E.S., Biretta J.A., Sparks W.B., et al. 1999, AJ 117, 2185
Pian E., Vacanti G., Tagliaferri G., et al. 1998, ApJ 492, L17
Polnarev A.G., Rees M., 1994, A&A 283, 301
Protheroe R.J., Bhat C.L., Fleury P., et al. 1998, in: Proc. of 25th International Cosmic Ray Conference (Durban) 8, p.317
Quinn J., Bond I.H., Boyle P.J., et al. 1999, ApJ 518, 693
Rees M., 1984, ARA & A 22, 471
Rees M., 1994, in: Muñoz-Tuñón C. & Sánchez F. (eds.), Observational Evidence for Black Holes in the Universe. Dordrecht: Kluwer, p. 157
Samuelson F.W., Biller S.D., Bond I.H., et al. 1998, ApJ 501, L17
Schramm K.-J., Borgeest U., Camenzind M., et al. 1993, A&A 278, 391
Sillanpää A., Haarala S., Valtonen M.J., et al. 1988, ApJ 325, 628
Sol H., Pelletier G., Asséo E., 1989, MNRAS 237, 411
Spada M., 1999, Astropart. Phys. 11, 59
Spada M., Salvati M., Pacini F., 1999, ApJ 511, 136
Stickel M., Fried J.W., Kühr H., 1993, A&AS 98, 393
Swain M.R., Bridle A.H., et al. 1999, ApJ 507, L29
Thorne K.S., Price R.H., Macdonald D.A. (eds), 1986, Black Holes: The Membrane Paradigm, Yale: Univ. Press
Villata M., Raiteri C.M., Sillanpää A., Takalo L.O., 1998, MNRAS 293, L13
Villata M., Raiteri C.M., 1999, A&A 347, 30
Wagner S.J., Lamer G., Bicknell G. V., 1999, Astronom. Nach. 320, 226
White S.D.M., 1997, in: Börner G., Gottlober S. (eds.), The Evolution of the Universe: Report of the Dahlem Workshop, (Berlin 1995), p. 227