Radiative transfer modelling of parsec-scale dusty warped discs

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ABSTRACT
Warped discs have been found on (sub-)parsec scale in some nearby Seyfert nuclei, identified by their maser emission. Using dust radiative transfer simulations, we explore their observational signatures in the infrared in order to find out whether they can partly replace the molecular torus. Strong variations of the brightness distributions are found, depending on the orientation of the warp with respect to the line of sight. Whereas images at short wavelengths typically show a disc-like and a point source component, the warp itself only becomes visible at far-infrared wavelengths. A similar variety is visible in the shapes of the spectral energy distributions. Especially for close to edge-on views, the models show silicate feature strengths ranging from deep absorption to strong emission for variations of the lines of sight towards the warp. To test the applicability of our model, we use the case of the Circinus galaxy, where infrared interferometry has revealed a highly elongated emission component matching a warped maser disc in orientation and size. Our model is for the first time able to present a physical explanation for the observed dust morphology as coming from the active galactic nuclei heated dust. As opposed to available torus models, a warped disc morphology produces a variety of silicate feature shapes for grazing lines of sight, close to an edge-on view. This could be an attractive alternative to a claimed change of the dust composition for the case of the nearby Seyfert 2 galaxy NGC 1068, which harbours a warped maser disc as well.

Key words: black hole physics – radiative transfer – methods: numerical – dust, extinction – galaxies: nuclei – galaxies: Seyfert.

1 INTRODUCTION AND MOTIVATION
Due to their vicinity, Seyfert galaxies have been the prime target to investigate the physics of active galactic nuclei (AGN). An integral part of our current understanding of AGN is a geometrically thick gas and dust structure – typically referred to as the molecular torus. A toroidal shape enables the orientation-dependent obscuration (Antonucci 1993; Urry & Padovani 1995), put forward to unify two observed classes of active galaxies: type 1 sources have direct lines of sight towards the centre and show both, narrow and broad emission lines and type 2 sources which show narrow emission lines only. The torus is also the reservoir of gas available for accretion onto a central supermassive black hole (SMBH) which is thought to power the central activity. A fraction of the emitted UV/X-ray is reprocessed into the IR wavelength regime by the dust, visible in the so-called IR-bump in their spectral energy distributions (SEDs). The idea of such a geometrically thick dust structure was coined after broad emission lines have been found in the polarized light of type 2 sources (e.g. Miller & Antonucci 1983; Antonucci & Miller 1985). This led to the interpretation that a type 1 nucleus is hidden inside type 2 sources by a dusty torus seen edge-on. Radiation is scattered towards the observer by free electrons and tenuous dust in the opening cone of the torus.

First direct evidence for the geometrical distribution of the dust was found by Jaffe et al. (2004) with the help of the mid-infrared interferometric instrument (MIDI; Leinert et al. 2003) at the Very Large Telescope Interferometer (VLTI). One of the best-studied parsec-sized dust distribution is harboured by the Circinus galaxy, which is the closest (4.2 Mpc, 1 arcsec ≈20 pc; Freeman et al. 1977) and the second brightest Seyfert galaxy in the MIR. High-resolution mid-infrared (MIR) interferometric observations have revealed a two-component morphology in the brightness distribution: (i) a larger scale, elongated component in direction of the ionization cone (along PA ≈107°) with a full-width at half-maximum (FWHM) size of roughly 0.8 × 1.9 pc, which is responsible for 80 per cent of the total MIR flux and was interpreted either as the directly illuminated funnel walls of the dusty molecular torus or as part of the filamentary/clumpy outflow; (ii) a disc-like component with an FWHM size of roughly 0.2 × 1.1 pc and elongated along PA ≈46° (Tristram et al. 2007, 2014). Both components have a dust temperature...
of roughly 300 K. The disc-like component was modelled by two Gaussian emitters (a highly elongated emitter plus an unresolved source) in the simple model used by Tristram et al. (2014). This was interpreted as signs for a more complex structure as well as for asymmetry in the second component. The orientation and size of the disc-like component coincides with an edge-on warped disc seen in maser emission with the help of very long baseline interferometry traced by H$_2$O masers (Greenhill et al. 2003). It has an outer radius of roughly 0.4 pc. A similar picture emerges for NGC 1068: A hot parsec-scale disc (FWHM $\approx$1.35 $\times$ 0.45 pc, $T \approx$ 800 K) was found with similar orientation and extent as the H$_2$O maser disc (Greenhill et al. 1996; Greenhill & Gwinn 1997). It is surrounded by warm dust extended in polar direction with an FWHM $\approx$3 $\times$ 4 pc and a temperature $T \approx$ 300 K (Jaffe et al. 2004; Raban et al. 2009). However, in a systematic study of a larger sample of objects a large range of properties of the dust distribution has been found (Burtscher et al. 2013).

As a first step to investigate the observational implications and to determine possible morphologies of AGN tori, geometrical toy models have been set up (e.g. Pier & Krolik 1992b; Granato & Danese 1994; Schartmann et al. 2005; Fritz, Franceschini & Hatziminaoglou 2006; Schartmann et al. 2008; Höning & Kishimoto 2010; Stalevski et al. 2012; Siebenmorgen, Heymann & Efstathiou 2015). Knowledge gained from this effort was used to set up physical models. These concentrated on the mass supply (Schartmann et al. 2009, 2010) and their dynamical stability (Wada & Norman 2002; Wada, Papadopoulos & Spaans 2009). Especially, the role of radiation pressure has gained substantial interest in the recent years (e.g. Krolik 2007; Schartmann, Krause & Burkert 2011; Dorodnitsyn & Kallman 2012; Wada 2012; Schartmann et al. 2014; Wada 2015; Chan & Krolik 2016; Wada, Schartmann & Meijerink 2016) following the early work of Pier & Krolik (1992a).

Alternative theories have postulated dusty winds to completely replace AGN tori (Emmering, Blandford & Shlosman 1992; Königl & Kartje 1994; Elitzur & Shlosman 2006). For a more thorough discussion of possible AGN torus models, we refer to Chan & Krolik (2016).

In this paper, we will concentrate on the observational appearance of geometrically thin, but warped discs. Although the idea was brought forward already more than 25 years ago by Sanders et al. (1989), it has thus far received only very little attention. Its main advantage is that a significant covering fraction of the sky can be reached without the need of having a large scaleheight. In this context, Lawrence & Elvis (2010) discuss misaligned discs as possible sources of AGN obscuration. Maser emission at 22 GHz has been found in a large number of nuclei in active galaxies (e.g. Kartje, Königl & Elitzur 1999). In some of the best-studied cases, they appear in warped disc structures, e.g. NGC 4258 (Greenhill et al. 1995; Herrnstein, Greenhill & Moran 1996), NGC 1068 (Greenhill et al. 1996; Greenhill & Gwinn 1997), NGC 3393 (Kontratko, Greenhill & Moran 2008) and the Circinus galaxy (Greenhill et al. 2003). Several physical mechanisms have been suggested to trigger the warping of discs, like e.g. radiation pressure induced warping instability (Maloney, Begelman & Pringle 1996; Pringle 1996), an orbiting massive object (Papaloizou, Terquem & Lin 1998), stellar torques from a nuclear star cluster (Bregman & Alexander 2012) or stellar rings (Nayakshin 2005), misalignment between momentum of infalling material and the spin of the central black hole or due to the presence of a binary black hole (e.g. Tremaine & Davis 2014).

Dust can play an important role in the thermodynamics of the maser pump cycle (Collison & Watson 1995). This together with measured inner radii of the maser emission close to the sublimation radius of dust makes the coexistence of gas and dust in these systems very likely.

The main aim of this publication is to do a first investigation of the observational consequences of dusty, warped discs in the (sub-) parsec scale environment of nearby Seyfert galaxies. Our standard model is one realization of a warped disc structure inspired by the properties of the nucleus of the Circinus galaxy, and we discuss the effects of varying its main morphological parameters. The underlying density distribution of the model and methods used are summarized in Section 2. The typical features of such a warped disc model will be presented in Section 3, a comparison with the Circinus galaxy is done in Section 4 and we will discuss benefits and shortcomings in Section 5. We summarize our work and draw our final conclusions in Section 6.

2 MODEL SETUP AND METHODS

2.1 The density of the disc

For the sake of simplicity, we adopt a geometrical model with a constant dust density for the disc around the central source. The inner radius of the disc is chosen such that the highest temperature to which the dust grains are heated is close to the sublimation temperature, which we assume to be 1500 K for our dust mixture (Fig. 1). The warping angle is chosen such to resemble the one derived by Greenhill et al. (2003) for the Circinus galaxy. As maser emission traces only the densest part of the disc, the choice of the other parameters of the model are motivated by MIR observations of the Circinus galaxy by Tristram et al. (2014), which include the value of the outer radius for which we adopt 3.15 pc. Together with the density of the dust, eight parameters characterize our model. In the following, we will explain the geometrical functions we use to build up the dust distribution. We first describe what we call the flat model and then explain how we apply the warp by changing the coordinate grid used to calculate the flat model.

The cross-section of the flat model is a wedge which has been modified to have a concave shape at small radii and which turns over at large radii (the cross-section of the flat model is identical to the cut shown in the middle panel of Fig. 2). We adopt a concave shape close to the source to resemble hydrostatic equilibrium configurations.
but also to have directly illuminated dust closer to the source. To generate the flat model, we first calculate the height of the disc according to the following function:

\[ h_b(r_{cyl}) = \frac{1}{5} r_{cyl} \tan(\xi), \tag{1} \]

where \( h_b \) is half of the disc thickness in the \( z \)-direction as a function of the cylindrical radius \( r_{cyl} \), i.e. the distance to the \( z \)-axis, and \( \xi \) is the opening angle of the wedge. Furthermore, we implement a minimal disc height of \( h_b(0) \) in the inner part to account for limitations in resolution. To get a concave shape of the disc close to the source, we make the opening angle \( \xi \) a function of the radius. The following function decreases the opening angle for values of \( r_{cyl} \) close to the inner \( (r_{in}) \) and outer \( (r_{out}) \) boundary of the disc:

\[ \xi(r_{cyl}) = \sin \left( \frac{r_{cyl} - r_{in}}{r_{out} - r_{in}} \right). \tag{2} \]

To flatten the disc and get closer to the shape expected from hydrostatic equilibrium, we finally apply the following function:

\[ d_{h}^{\text{final}}(r_{cyl}) = d_b(r_{cyl}) \sin \left( \frac{r_{cyl} - r_{in}}{r_{out} - r_{in}} + \frac{\pi}{2} \right)^8. \tag{3} \]

To warp the disc, we change the \( z \)-coordinates of our coordinate grid, which we use to calculate the flat model described above. We warp the disc in the \( z \)-direction with maximum amplitude in the \( xz \)-plane from an inner radius which we denote by \( r_{w_{in}} \) to an outer radius \( r_{w_{out}} \). The new coordinate \( \tilde{z} \) is given as follows:

\[ \tilde{z}(x, y, z) = z + z_w \sin \left( \frac{\pi}{2} \frac{x - \text{sgn}(x) x_d}{r_{w_{out}} - r_{w_{in}}} \right), \tag{4} \]

where \( z_w \) parametrizes the largest possible dislocation. We smoothly decrease the warp as we approach the \( y \)-axis to end up with no warp at all in that direction, which we parametrize by

\[ x_d(x, y) = \frac{r_{w_{in}}}{r_{cyl}} x. \tag{5} \]

Furthermore, \( \text{sgn}(x) \) denotes the sign of the coordinate \( x \). Finally, we cut out the dust lying outside the spherical shell limited by the radii \( r_{w_{in}} \) and \( r_{w_{out}} \) and continue the non-warped disc smoothly outside the warp-region defined by \( r_{w_{in}} \) and \( r_{w_{out}} \). The parameters we use for our calculations are given in Table 1. Furthermore, a visualization of the 3D temperature distribution for our standard model is shown in Fig. 1. Its outer contour corresponds to the shape of the dust distribution.

The restriction to a model with constant density allows us to circumvent limitations in the achievable spatial resolution and optical depth of the modelling. For a disc in hydrostatic equilibrium around a central SMBH, a steep density gradient around the equatorial plane would be expected (e.g. Pringle 1981). This means that the total mass given in Table 1 is probably underestimating the real mass. However, the inner part of our distribution’s morphology roughly follows the outer shape of such a flared disc geometry.

2.2 The radiative transfer approach

For our simulations, we use the 3D dust continuum radiative transfer capabilities of \texttt{RADMC-3D} \footnote{http://www.ita.uni-heidelberg.de/~dullemond/software/radmc-3d/} (version 0.39_17_03_15). The code is
based on the Monte Carlo approach and allows us to first compute
the dust temperature. We can then use this temperature distribution
as an input for the calculation of the SEDs, after specifying a central
source and the characteristics of the dust grains. \textsc{radmc-3d} computes
the dust temperature by dividing the total luminosity of the source
into \( n_{\text{photon}} \) packages, which are then emitted by the source one at
a time. Moving through the coordinate grid they may scatter or
be absorbed by the dust grains according to the absorption and
emission coefficients specified. In going through the grid, each
photon package entering a cell increases the cell’s energy and in
turn also the dust temperature associated with that cell. The final
dust temperature is obtained once all photon packages have escaped
and an equilibrium has been reached. As an approximation, we only
use the isotropic scattering mode of the code. Furthermore, the only
effect scattering can have is changing the direction of a photon. In a
second step, we can then use the ray-tracing capabilities of \textsc{radmc-
3d} to make images and spectra. For these computations, a transfer
equation containing a scattering source function has to be integrated
for each pixel, where the integration goes along the one-dimensional
ray belonging to that pixel. However, to do that one has to know
the scattering source function, which \textsc{radmc-3d} computes through a
so-called \textit{scattering Monte Carlo} run for a single-wavelength. The
number of photon packages we use for the scattering Monte Carlo
simulation is \( n_{\text{photon}} = 10^7 \) for both the creation of images and
spectra, if not explicitly stated otherwise.

For our simulations of the warped model, we use a three-
dimensional Cartesian coordinate grid consisting of 320 cells in
each direction ranging from \(-3.2\) to \(3.2\) pc. We use an equally spaced grid which results in a cell volume of \( v_c = 8 \times 10^{-6} \) pc\(^3\). We also performed simulations for the flat model, which we could implement
in a two-dimensional spherical coordinate system exploiting
the symmetry. This enabled us to run simulations at a higher spatial resolution. A comparison with our standard Cartesian grid
simulations showed that the results are sufficiently converged for
our conclusions. The results for the flat model shown in Section 4.2
are based on a uniform grid with 320 values in radial direction \( R \in \left[0.01, 3.2\right]\) pc and 192 values for the polar angle \( \theta \in \left[0, \pi\right] \). The
flat model is generated with the same parameters and procedure
as we use in the warped case just without applying the warp. For the
computation of the SEDs, we choose a logarithmic wavelength grid
with values of \( \lambda \in \left[0.001, 2000\right] \mu\text{m} \). The range has been divided
into three regions, with 20 logarithmically spaced values in the
interval \( [0.001, 2] \mu\text{m} \), 140 in \([2, 25] \mu\text{m}\) and 30 in \([25, 2000]\) \mu\text{m}.
An overview over the input parameters we use is given in Table 1.

2.3 Central source and dust characteristics

We assume the dust to be heated by a central accretion flow sur-
rounding a black hole and approximate its emission by an isotropic,
central, point-like energy source. We used isotropic emission in
order to prevent us from having to make any specific assumption
about the orientation of the accretion disc. As it turns out, our gen-
eral results are not affected by this choice (see the discussion in
Section 5). We set the central source luminosity to \( 1.64 \times 10^{40} \) L\(_\odot\),
which corresponds to 30 per cent of the Eddington luminosity for
a black hole mass of \( 1.7 \times 10^6 \) M\(_\odot\) as derived for the Circinus
galaxy by maser disc kinematics (Greenhill et al. 2003). This is in
accordance with the findings of Tristram et al. (2007), who derive a
luminosity of \( 10^{40} \) L\(_\odot\). The SED of the source is shown in Fig. 3 and

A typical galactic dust model is used, similar to the one presented
in Schartmann et al. (2005). We set up a mixture of 62.5 per cent
silicate grains and 47.5 per cent of graphite grains (taking the two
possible orientations of the optical axis into account), distributed
according to a grain size distribution following Mathis, Rumpl &
Nordsieck (1977). Optical constants are taken from Draine & Lee
(1984), Laor & Draine (1993) and Weingartner & Draine (2001).
With these ingredients, we calculate an average dust model follow-
ing the approach of Wolf (2003).

3 Characteristic appearance

In the following, we present the main results of our work obtained
using the radiative transfer code \textsc{radmc-3d} with the density distri-
bution as described in Section 2.1. We will interpret images for
different lines of sight and wavelengths as well as the corresponding
SEDs to characterize our standard model and discuss consequences
of parameter variations. All SEDs we show in this paper include
both the dust re-emission spectra as well as the radiation from the
central source, which is added by \textsc{radmc-3d} in a post-processing step (i.e. to the image first rendered without the source, the flux
obtained by a ray tracing from the source to the observer is added
at the correct position, only taking extinction into account).

3.1 The temperature distribution

The temperature distribution of our standard model is shown in
Figs 1 and 2, where the temperature of all cells which contain no dust
has been set to zero. The highest temperature to which the dust is
heated is 1560 K, which is approximately the assumed sublimation
temperature of the dust. The three panels in Fig. 2 show cuts through
the temperature distribution along the coordinate planes. In the left-
hand panel, which shows a cut along \( y = 0 \), one can see the effect
of the warp in the \( z \)-direction, depending on the \( x \)-coordinate as

Figure 3. SED of the central heating source, which is assumed to radiate
according to a broken power law. Normalization is for a distance of 1 pc.

\[
\lambda F_\lambda \propto \begin{cases} 
\lambda^{1.2} & 0.001 \leq \lambda \, \mu\text{m}^{-1} < 0.01 \\
\lambda^0 & 0.01 < \lambda \, \mu\text{m}^{-1} \leq 1 \\
\lambda^{-0.5} & 1 < \lambda \, \mu\text{m}^{-1} \leq 5 \\
\lambda^{-3} & 5 < \lambda \, \mu\text{m}^{-1} \leq 50.
\end{cases}
\]
explained in Section 2.1. The flat disc inside the start of the warp at \( r_{\text{min}} \), as well as the final angle w.r.t the \( x \)-axis can clearly be seen. Due to the warping of the disc, the temperature distribution is clearly asymmetric as only one side can be illuminated directly from the central source.

Rotating the cut towards the \( yz \)-plane, the warp is slowly reduced to zero. The cut along the \( yz \)-plane is plotted in the middle panel and shows no difference to a cut one would obtain for the flat model. Finally, in the right-hand panel, the temperature distribution of the \( xy \)-plane is shown. In this plot, one can also observe the effect of the warp. Without a warp, the plot would show a spherical shell limited by the inner and outer radii of the dust distribution. However, here we see that the dust distribution is warped out of the plane towards negative – respectively positive \( z \) values depending on the \( x \)-coordinate. The effect of the flat inner disc can also be seen as most of the dust heated to the highest temperatures still lies inside this plane.

### 3.2 Images at various lines of sight

In the following, we show images of our standard model for different inclinations \( \theta \) and rotation angles \( \phi \) taken at a wavelength of 12 \( \mu \)m. The angles specify the location of the observer, where the inclination is measured from the \( z \)-axis and may be characterized by two vectors. One of these vectors points along the negative \( z \)-axis, corresponding to \( \theta = 0^\circ \), the other one, associated with \( \theta = 90^\circ \), lies in the \( z = 0 \) plane. The rotation angle rotates the location of the observer clockwise around the \( z \)-axis, i.e. the model is rotated counterclockwise w.r.t the observer. Therefore, for a flat model one would obtain a face-on view for an angle of \( \theta = 0^\circ \), corresponding to an extreme Seyfert 1 case. An edge-on view and thus an extreme Seyfert 2 case would be seen for an angle of \( \theta = 90^\circ \). In our warped model, the geometry is somewhat more elaborate and it is thus not possible to define an explicit edge–or also face-on views as there are always parts of the dust which may be directly illuminated or obscure the central source.

In Fig. 4, we show images at a wavelength of 12 \( \mu \)m for inclinations of \( \theta = 45, 90 \) and \( 135^\circ \) and rotation angles of \( \phi = 0, 45, 90 \)and\( 135^\circ \). The models possess point symmetry, which means that we get the same image for angles of \( \theta = 45^\circ \), \( \phi = 0^\circ \) and \( \theta = 135^\circ \), \( \phi = 180^\circ \) up to a reflection at the horizontal axis. The upper row shows an inclination angle (slightly) outside the opening angle of the disc. Hence, a large fraction of the directly illuminated part of the disc is visible for all rotation angles \( \phi \). The leftmost image is viewed along the direction of the strongest warp with an almost grazing line of sight w.r.t. the warp in the positive \( z \)-direction (compare to Figs 1 and 2). With increasing rotation angle \( \phi \), a larger and larger fraction of the directly illuminated surface of this upper warp is visible and a characteristic pear-shaped structure appears. The same behaviour is observed when the model is viewed from below the \( z = 0 \) plane (lower row). Due to the point symmetry, the lower row of Fig. 4 can be thought of a continuation of the rotation shown in the upper row. All images appear elongated in direction of the main warp.
Dependence of the SEDs of our standard model on different lines of sight for three inclination angles and dotted black to 135°. Much larger appearance and to the asymmetric case. The deepest absorption in the middle row of Fig. angles is identical for the two categories: (i) strongly warped discs (left-hand panels of Figs 7a and b) that extend far from the xy-plane and (ii) minor warps which remain close to the flat model (right-hand panels of Figs 7a and b).

Concerning the SEDs under an inclination angle of 45° (Fig. 8, left-hand panel), all parameter changes lead to minor changes in the SEDs, as for this inclination angle all lines of sight are within the dust-free region. Therefore, this also applies to smaller inclination angles and differences are only expected due to the inner rim of the unwarped, central disc. The exception are the models with zw = 1.0 pc, ζ = 0.8 and rwo = 1.2 pc and rwo = 0.25 pc and 0.5 pc which extend furthest in the z-direction (Fig. 7, blue dashed and black long-dashed lines). In this case, some of the lines of sight are now able to intersect with cold dust, leading to partly strong extinction, substantially decreasing the flux shortwards of 50 µm. Hence, the range of SEDs for various φ angles increases a lot towards lower energy output. This can be seen for the SEDs of the model with zw = 1.0, ζ = 0.8 and rwo = 1.2 for the line depth decreases when rotating the model towards a view along the direction of the strongest warp (blue solid line, φ = 0°) as then the largest fraction of the directly illuminated inner surface of the disc is exposed. The latter leads to a silicate feature in self-absorption (Henning 1983). This means it is combined with an emission feature from these exposed surfaces, leading to a narrower silicate feature in absorption, which is slightly shifted to shorter wavelengths (see discussion in Section 4).

3.4 Parameter dependences of the model

In order to get an idea of the parameter dependences of our model, we ran a series of simulations by changing each of the parameters defining the warp morphology by a factor of 2 with respect to our standard model, resulting in 16 simulations (see Table 1). The change of the dust distribution is demonstrated in Fig. 7. The strongest change in the warp morphology is visible for changes of rwo. A larger value leads to a weaker warp – or a smaller shift in the z-direction, respectively, e.g. compare the green dotted line to the blue dashed line in Fig. 7(a). A similar effect can be reached with the parameter ζ, but in opposite direction (compare the green dash–dotted to the blue dashed line). Small differences arise due to the additional change of the range of the warp and the corresponding smooth continuation beyond rwo. Parameter ζ scales the warp function, partly leading to sharp edges towards the inner unwarped region. rwo has a minor effect on the overall warp, only defining the width of the inner, unwarped disc (compare the blue dashed with the black, long-dashed line). Hence, other models with rwo = 0.5 are not discussed further. Overall, the simulations can be split into two categories: (i) strongly warped discs (left-hand panels of Figs 7a and b) that extend far from the xy-plane and (ii) minor warps which remain close to the flat model (right-hand panels of Figs 7a and b).

3.3 Spectral energy distributions

In Fig. 6, we show the SEDs of our standard model corresponding to the position of the observers as chosen for the images in Fig. 4. All SEDs shown in this section are normalized to a distance of 1 pc.

As already mentioned during the discussion of the images (Section 4), an inclination angle of θ = 45° allows a direct view of the central directly illuminated part for all rotation angles as well as the cold dust in the outer part of the warped disc, resulting in a comparatively broad IR SED. In addition, the characteristic silicate features at 9.7 and 18.5 µm are visible in emission only. As already discussed in Granato & Danese (1994), all viewing angles outside the dusty disc or torus will result in very similar SEDs. This is confirmed by the various lines in the last panel of Fig. 6. Due to the point symmetry of the model, the shaded region which summarizes the range of φ angles is identical for the two θ angles. Much larger variations are visible for the θ = 90° case. The deepest absorption feature is seen for lines of sight perpendicular to the warp direction (green dot–dashed line, φ = 90°), due to the large column density along the line of sight and thus a high extinction rate. The feature

\[ \frac{2}{m} \text{pc and self-absorption} \]

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\[ \text{in absorption, which is slightly shifted to shorter wavelengths (see discussion in Section 4).} \]
Figure 7. Limiting density contours within the $xz$-plane (left-hand panels) and $xy$-plane (right-hand panels) for part of the models of our parameter study (line styles as given in the legend). In the left half of the panels, the models which are classified as strongly warped are plotted whereas the right half of the panels show the weakly warped models. Changing $r_{\text{win}}$ has only minor effect on the morphology and observables. Hence, only one example is shown (see the text for details).

Figure 8. SEDs of the different models of our parameter study for two inclinations, $\theta = 45^\circ$ and $\theta = 90^\circ$. Shaded in grey are the SEDs of all weakly and strongly warped models for rotation angles of $\phi = 0^\circ$ and $\phi = 90^\circ$ (only in the right-hand panel) except the two models characterized by $z_w = 1.0$, $r_{\text{win}} = 0.25$, $r_{\text{wout}} = 1.2$ pc, $\zeta = 0.8$ and $r_{\text{win}} = 0.5$ pc. The SEDs corresponding to these models are represented by the blue lines for $r_{\text{win}} = 0.25$ pc, solid for $\phi = 0^\circ$ and dotted for $\phi = 90^\circ$, respectively, by the black lines for $r_{\text{win}} = 0.5$ pc (dash–dotted: $\phi = 0^\circ$, dashed: $\phi = 90^\circ$). In addition in the right-hand panel, all SEDs, except the two mentioned before, of the strongly warped models are represented by the green lines and those of the weakly warped models by the red lines for a rotation angle of $\phi = 0^\circ$.

For lines of sight along the $x$-axis ($\phi = 0^\circ$, parallel to the direction of the strongest warp), we find a dichotomy: the mildly warped models all show the silicate feature in absorption only (red lines in Fig. 8) and do not show significant differences for the change in $r_{\text{win}}$. The reason being that there is always some cold dust along the line of sight. Only those models exhibiting a strong enough warp such that some $\phi$ angles allow direct lines of sight towards the inner, unwarped disc show a larger variety of SEDs. This also leads to a significant difference when changing the inner warp radius, as $r_{\text{win}} = 0.25$ allows direct views towards hot dust, resulting in the silicate feature to appear in emission. This parameter study is meant to give a rough impression of the importance of the strength of the warp. As for any geometrical toy model, there is a large amount of degeneracy that significantly impacts on the resulting SEDs and images (see discussion in Section 5).

4 COMPARISON TO THE CIRCUINUS GALAXY

In this section, we apply our warped standard model to the specific case of the Circinus galaxy and compare it with observations by Tristram et al. (2014). Our goal is not an accurate modelling of these observations, but rather to qualitatively assess the applicability and limitations of the model at hand. For the comparison with the Circinus galaxy SED, we assume a distance of 4.2 Mpc in accordance with Freeman et al. (1977). As already mentioned, Tristram...
et al. (2014) find that the interferometric data in the MIR is best described by a two-component model of the brightness distribution. It is composed of a diffuse large-scale component, which seems to be associated with the ionization cone and narrow-line region and an elongated, elliptical, disc-like component, which includes a surface brightness concentration that is offset from the centre. Here, we are only interested in the disc-like component, which – when combined with the maser emission data – might be explicable by a warped disc. To this end, we will limit our discussion in the following to a comparison of the modelled brightness distribution as well as the modelled SEDs of the point source plus disc-like component from Tristram et al. (2014), which can be separated by comparing to certain baseline configurations of the interferometer. We also discuss the corresponding geometrically flat model in order to examine the differences with respect to the warped case.

4.1 Warped case

For our standard model, we find the best comparison to the data for an observer with a line of sight described by an inclination of \( \theta = 70^\circ \) and \( \phi = 60^\circ \), corresponding to an almost grazing line of sight. The total dust mass in the model was adjusted to obtain a good correspondence to the silicate feature depth in the MIDI correlated flux spectrum. The inclination angle of \( \theta = 70^\circ \) is in agreement with the inclination angle of the galactic disc of the Circinus galaxy (\( i = 65^\circ \); Freeman et al. 1977). However, Greenhill et al. (2003) estimate a roughly edge-on orientation as the masers form a tight spatial sequence. In the leftmost plot of Fig. 9, we show the MIR emission at a wavelength of 12 \( \mu m \) for this observer position. We choose a logarithmic scale for the intensity such that also fainter parts of the disc can be seen. Looking only at the high-intensity regions, we can observe a three-component structure: (i) the warped regions which are directly illuminated by the central source are only visible partially. They hence appear as an elongated disc-like structure which is asymmetric and displaced to the lower right with respect to the position of the central source. No direct signs of a warped density distribution are visible in this intensity map. (ii) A brightness concentration within this disc, which is offset to the upper left and (iii) a much fainter blob component reflecting the innermost part of the directly illuminated warp and is located very close to the heating
source. Neglecting the latter which only contributes approximately 1–2 per cent of the total flux, this is in accordance to the disc component together with the point-like concentration of the model by Tristram et al. (2014). Despite being a crude first model, the flux contribution of the disc (≈70–75 per cent) and point source (≈25–30 per cent) w.r.t. the sum of both is in reasonable agreement with the model presented in Tristram et al. (2014), who find values of 70 per cent and 30 per cent, respectively. Mind that the MIDI observations described there do not allow for accurate positioning of the components. Especially, the point source component should rather be regarded as a hint towards an asymmetric distribution in the disc-like component. In the context of our warped disc model, we hence interpret the asymmetric disc in the visibility data as evidence for a warped dust distribution. Another interesting prediction of our model is the offset of the disc-like component in the north-west direction by approximately 20 mas with respect to the galactic nucleus.

Maser emission from our model is expected along the lines of sight with the largest optical depth. The distribution of the optical depth at 12 μm for the same inclination and rotation angle is shown in the middle panel of Fig. 9 and clearly shows a warped disc morphology. Therefore, our choice of the dust distribution and line of sight seems to be able to simultaneously account for the MIR interferometric results, as well as a warp similar to the maser disc geometry. Finally, in the right-hand panel of Fig. 9, we show the corresponding SED as the black solid line, together with the model of Tristram et al. (2014) and high spatial resolution observations compiled by Prieto et al. (2010). The VLTI/MIDI observations allow us to disentangle the nuclear MIR emission. At a position angle of roughly 125° and a projected baseline length of roughly 60 m, the extended component is essentially resolved and the disc component is essentially unresolved. The observed correlated flux at this position in the (u,v) plane can therefore be considered as emission only from the disc plus point source component (red dotted line; Tristram et al. 2014), which is in reasonable agreement with our simulation. The overall scale of our modelled SED is lower than the single-dish observations (filled dots), which is understandable given the small covering factor of our disc and 80 per cent of the total MIR flux coming from the extended emission component in Tristram et al. (2014).

To better characterize the model, we show images for different wavelengths and the same line of sight (θ = 70°, φ = 60°) in Fig. 10. In the leftmost plot, where we show an image in the visible range of the spectrum (0.5 μm), we only see a disc-like structure which seems to be broken up into two components. The L-band (3.5 μm) image in the second panel looks more similar to the 12 μm image discussed before (and shown in the third panel). However, tracing the emission from hotter dust, the central region is more pronounced in the 3.5 μm image compared to longer wavelengths. Only a small fraction of the directly illuminated warp of the disc reaches temperatures high enough to be visible in the L band. This suggests that images reconstructed from upcoming MATISSE (Lopez et al. 2014) L-band observations might be dominated by a point source component. The rightmost panel corresponds to an image at an FIR wavelength of 500 μm. Interestingly, the structure changes significantly and our model predicts that the warp should be recoverable with Atacama Large Millimeter Array observations, which in the most extended configuration of 16 km will reach a spatial resolution of roughly 8 mas. However, one should keep in mind that our model does not include the large-scale component along the ionization cone, which might contribute significantly.

To emphasize that our model shows a large variety of SEDs and feature shapes even for small changes in the line of sight, we show in Fig. 11 a close on view on the wavelength range containing the characteristic silicate features for observers at a location around the best-fitting angles. As we see in this plot, the shape of the feature at 9.7 μm changes noticeably even for small variations of the φ angle (the same is true for changes in the θ angle). We see that the features for φ = 50° (dot–dashed green) and φ = 70° (dotted blue) show both a different shape and a different strength as compared to the best-fitting angles. This strong dependence on the line of sight is associated with the complex geometry of our warped disc for viewing angles close to grazing lines of sight. Only a small change in viewing direction can significantly decrease the column density or increase the amount of directly illuminated dust observed. This has the effect that an absorption feature is filled up from the long wavelength end (by adding emission components), resulting in a change of the feature towards longer wavelengths. The latter effect is independent of the geometrical distribution, but the shift of the minimum (or maximum in the case of an emission feature) happens
when the optical depth of the dust in-between the source and the observer changes. Interestingly, for our model geometry, this happens for grazing lines of sight at inclinations for which we also reach the best agreement with the observations of the Circinus galaxy. This is not easily the case for a doughnut-like structure. A similar difference of the silicate feature shape w.r.t. the absorption profile for a typical galactic dust mixture has been seen in the nearby Seyfert 2 galaxy NGC 1068 (Raban et al. 2009). They found that an absorption profile with a shallower slope towards longer wavelengths compared to the standard galactic one is needed in order to be able to explain their MIDI observations (see fig. 5 in Raban et al. 2009).

Our study shows that a significant change can already be obtained in a flat disc geometry when slightly changing the observing direction around grazing lines of sight (see also Section 4.2). This geometrical effect could provide an alternative (and probably more natural) explanation for the seemingly unusual shape of the silicate feature found in NGC 1068, which harbours a warped maser disc as well. In contrast, the observed silicate feature in the Circinus galaxy can be well explained by a standard galactic dust mixture and is at odd with our best-fitting model. Viewing angles with more dust along the line of sight result in a better match, e.g. viewing along $\theta = \phi = 90^\circ$ (green dot–dashed line in Fig. 6). The same effect could also be obtained by adding an absorption screen, which could be provided by the missing large-scale component. In Fig. 11, we also show the SED for an observer characterized by $\theta = 70^\circ$ and $\phi = 0^\circ$. Even though the depth of the feature at $9.7 \mu m$ is of comparable size to the best-fitting model, it shows a different shape, which is specific to our choice of warped disc geometry. From a flat model, we would expect that the change in shape is always also accompanied by a change in the depth of the feature. The reason being that we have only one free parameter characterizing the line of sight. Therefore, we always change the column density along the line of sight and thus the depth of the feature by changing this parameter.

### 4.2 Flat case

In Fig. 12, we show the same type of plots as in Fig. 9 but for the case of an unwarped disc with otherwise unchanged parameters. The line of sight which fits best the model of Tristram et al. (2014) is in the flat case described by an inclination angle of $\theta = 80^\circ$. We plot the MIR emission at a wavelength of $12 \mu m$ in the left-hand panel of Fig. 12(a). The basic structures we observe are a dominating elongated disc-like component and a much fainter point source. Due to symmetry and in contrast to the warped case, the disc does not possess any substructure or asymmetry that could be associated with the point source component of the MIDI models. Clearly, we see in the middle panel of Fig. 12(b) that the optical depth distribution has a perfectly flat major axis and – of course – no traces of a warp in the maser emission are expected to be seen. Nevertheless, the line of sight can be chosen such that we can find accordance in the SED with the model by Tristram et al. (2014) when restricting to the disc and point-like component, as shown in Fig. 12(c). If we compare the shape of the silicate features to Fig. 11, we see that in the flat case the feature changes its shape as well. However, as we have only one free parameter describing the line of sight in the flat case, we cannot find two lines of sight with comparable feature depth but completely different shape in the SED around the feature.

Figure 11. Close-on view on the part of the SEDs of our standard model corresponding to the wavelengths associated with the silicate features. We draw in solid black the line of sight corresponding to our best-fitting model ($\theta = 70^\circ$, $\phi = 60^\circ$) together with two lines of sight corresponding to $\phi = 50^\circ$ (dot–dashed green) and $\phi = 70^\circ$ (dotted blue) for the same inclination. Furthermore, we show the SED for an observer characterized by $\phi = 0^\circ$ and $\theta = 70^\circ$ (dashed red). The region between the minimal and maximal values obtained for the SEDs in the range described by the angles $\theta = 70^\circ$ and $\phi \in [0^\circ, 180^\circ]$ with a step size of $10^\circ$ is shaded in grey. We normalized the SEDs to a distance of 4.2 Mpc. Various silicate feature shapes can be found depending on the orientation.

Figure 12. The best comparison of the flat model (corresponding to our standard model) to the Circinus observations is reached for a line of sight with $\theta = 80^\circ$ and $\phi = 0^\circ$. Panel (a) shows an image at $12 \mu m$, which has been rotated to fit the appearance on the sky (compare to fig. 7 in Tristram et al. 2014). In panel (b), we plot the optical depth at $12 \mu m$ for the same orientation. Panel (c) shows the SED corresponding to $\theta = 80^\circ$ in solid black and we overlay the same observations as in Fig. 9. Within the region shaded in grey lie all SEDs with lines of sight described by $\theta \in [0^\circ, 90^\circ]$ with a step size of $10^\circ$. The SEDs are normalized to a distance of 4.2 Mpc.
5 DISCUSSION

The results we present resemble available observations of warped discs in many respects, e.g. when looking at the SED (restricted to the small-scale disc and point source component) and the geometrical implications as derived from MIDI observations.

For our calculations, we assumed an isotropically emitting central source. However, a geometrically thin, optically thick accretion disc would lead to an anisotropic emission, where the flux depends on the polar angle $\theta$ as $F \propto \cos \theta (1 + 2 \cos \theta)$ (e.g. Netzer 1987). This would imply a stronger emission in direction of the disc axis, while the emission in direction of the plane would be reduced (Manske, Henning & Men’shchikov 1998; Schartmann et al. 2005). However, the orientation of the inner accretion disc with respect to our dust structure is unclear, especially for asymmetric discs as in the case of a warp. To this end, an isotropically emitting source seems to be most appropriate for this first study of warped disc geometries. Given the large inclination angles used for our comparison, we expect only a minor change of the short wavelength end of the SED (Fig. 12; Schartmann et al. 2005).

Another point for discussion is the large degeneracy we introduce with our dust distribution with a total of eight parameters. This means that we can achieve a large variety of different disc geometries and emission characteristics, sometimes producing the same overall predicitions even with quite different parameters (see Section 3.4). In addition, by choosing the line of sight appropriately, we observe large differences in the observed spectra. In this first approach towards studying warped discs as alternatives or amendments of classical torus models, we want to concentrate on general properties and whether such discs might be able to describe some of the peculiar properties of the Circinus galaxy. However, there may be a better combination of parameters and line of sight to explain the observations. Given the promising results of the phenomenological model presented here, a more detailed investigation of possible structures of warped discs and possible physical mechanisms which might cause such warps would be worth investigating further.

In addition, due to the constant dust density the calculations are simpler and we achieve converged results for a lower spatial resolution of the coordinate grid. Nevertheless, in a more physical approach, there would likely be a density gradient along the radial direction (e.g. Schartmann et al. 2005). However, as the break of axisymmetry in warped discs requires 3D simulations, we currently cannot achieve sufficiently converged results for the case of a steep density gradient. Therefore, one would either need a larger overall resolution or refine the grid in the inner regions of the torus where the dust is heated to the highest temperatures.

The simulations presented here are a first study of the influence of warped disc geometries on observable quantities. We neglect several things: (i) there are many indications that tori need to be clumpy. For the sake of simplicity, we concentrate on smooth dust distributions within warped geometric discs in this study. Changing this into a clumpy distribution will affect the shape of the silicate feature (Nenkova, Ivezic & Elitzur 2002; Hönig et al. 2006; Schartmann et al. 2008) and the SEDs in general. (ii) Taking grain-dependent sublimation into account has been shown to have a significant effect, especially for the short wavelength end of the IR bump (Schartmann et al. 2005). We defer these modifications to future work. This might include the combination of the simulations of this paper with the larger scale structure found in a recent radiation hydrodynamical simulation of the core of the Circinus galaxy (Wada et al. 2016).

6 SUMMARY AND CONCLUSIONS

In this paper, dust continuum radiative transfer calculations have been presented to characterize the observable signatures of dusty warped discs in the infrared. Our main results can be summarized as follows.

(i) Depending on the orientation of the warp with respect to the line of sight, we find strong variations of the brightness distributions. The geometry of the underlying warped density distribution can only be recovered at long wavelengths, whereas short wavelengths typically show thin discs and point sources in the brightness distribution.

(ii) Applying the models to the best-studied case of the Circinus galaxy, we find that a dust density distribution in form of a warped disc is able to account for the inner disc-like emission component revealed by MIDI observations. The warped disc geometry results in an asymmetric appearance (with respect to the central black hole) of the disc-like component for an inclination angle of around $70^\circ$. The best-fitting inclination needs to be close to a grazing viewing position and is in agreement with what is inferred for the galactic disc of the Circinus galaxy by other measurements as well. Also the point source component arises naturally on the visible, directly illuminated side of the warped disc structure and is offset from the centre point. This is in line with the original interpretation of the point source being part of an asymmetric disc, as its location could not be very well determined. The optical depth/column density distribution at this orientation clearly shows a warped disc geometry (Fig. 9b). This represents the highest probability for maser emission in our model, which was chosen to resemble this observed warp geometry. At the same viewing angle, the dust emission maps in the MIR (Fig. 9a) resemble a very thin, extended structure. No signs of the underlying warped disc geometry can be found in the emission in this wavelength range.

(iii) For the same orientation of the disc, we find qualitative agreement of the simulated SED with the MIDI correlated flux spectrum corresponding to a long baseline, which is mostly sensitive to the disc emission, excluding the large-scale component mentioned before.

(iv) The disc orientation has significant influence on the spectral shape of the silicate feature for grazing lines of sight, resulting in a change of slope towards the long wavelength end of the feature. This is reminiscent of MIDI correlated flux spectra of the Seyfert 2 galaxy NGC 1068, which harbours a (slightly) warped disc component on parsec scale as well. Thereby, it provides an alternative explanation to the claim of a non-standard dust composition in this nucleus.

Overall, the simulations indicate that a central, parsec-scale, warped, dusty disc provides remarkable features identifiable in some high-resolution observations of nearby Seyfert galaxies, which make it an attractive amendment to classically assumed AGN torus or newly established outflow morphologies.

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