ON THE RELATIONSHIP BETWEEN THE CORONAL MAGNETIC DECAY INDEX AND CORONAL MASS EJECTION SPEED

YAN XU, CHANG LIU, JU JING, AND HAIMIN WANG

Space Weather Research Lab, Center for Solar–Terrestrial Research, New Jersey Institute of Technology, 323 Martin Luther King Boulevard, Newark, NJ 07102-1982, USA; yx2@njit.edu

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ABSTRACT

Numerical simulations suggest that kink and torus instabilities are two potential contributors to the initiation and prorogation of eruptive events. A magnetic parameter called the decay index (i.e., the coronal magnetic gradient of the overlying fields above the eruptive flux ropes) could play an important role in controlling the kinematics of eruptions. Previous studies have identified a threshold range of the decay index that distinguishes between eruptive and confined configurations. Here we advance the study by investigating if there is a clear correlation between the decay index and coronal mass ejection (CME) speed. Thirty-eight CMEs associated with filament eruptions and/or two-ribbon flares are selected using the Hα data from the Global Hα Network. The filaments and flare ribbons observed in Hα associated with the CMEs help to locate the magnetic polarity inversion line, along which the decay index is calculated based on the potential field extrapolation using Michelson Doppler Imager magnetograms as boundary conditions. The speeds of CMEs are obtained from the LASCO C2 CME catalog available online. We find that the mean decay index increases with CME speed for those CMEs with a speed below 1000 km s⁻¹ and stays flat around 2.2 for the CMEs with higher speeds. In addition, we present a case study of a partial filament eruption, in which the decay indices show different values above the erupted/non-erupted part.

Key words: Sun: activity – Sun: coronal mass ejections (CMEs) – Sun: filaments, prominences – Sun: magnetic topology

Online-only material: color figure

1. INTRODUCTION

A coronal mass ejection (CME) is a sudden large-scale eruption from the solar surface to interplanetary space. The total mass carried by a CME could reach the order of 10^{13} kg (Chen et al. 2001), and the observed speed is as high as 3387 km s⁻¹, according to the online catalog by LASCO. The outward ejections contain not only massive plasmas but also magnetic fields. An Earth-oriented CME can disrupt Earth’s magnetosphere or even cause disruptions as deep as Earth’s surface.

Statistical studies (Moon et al. 2002; Jing et al. 2004) have found that CMEs are often associated with other phenomena of solar activity, such as filament eruptions and solar flares. From a theoretical perspective, they are now believed to be different manifestations of a single eruptive event (e.g., Priest & Forbes 2002) in which magnetic reconnection is a key process. In an equilibrium state, a filament may be supported by the magnetic flux rope (Antiochos et al. 1999; Fan & Gibson 2007; Török & Kliem 2005). However, the kink and torus instabilities, determined by the core field of the magnetic flux rope and overlying field (called the strapping field), could cause filaments to erupt. The kink instability is measured by the number of magnetic twists. When a twist exceeds a certain threshold, for instance, 2.5π to 3.5π (Hood & Priest 1981; Fan & Gibson 2003; Török et al. 2004), its filament would become unstable and eruptive. On the other hand, filament eruptions can also be triggered by torus instability, as a result of broken Shafranov equilibrium when the field strength decreases faster (Kliem & Török 2006; Török & Kliem 2005). In this respect, knowledge of the gradient of the strapping field is crucial for understanding the physical mechanisms of solar eruptive events.

To quantitatively describe how fast the strapping field decays, a decay index is defined as \( n = -d \log(B_t)/d \log(h) \) (Kliem & Török 2006), in which \( B_t \) is the strength of the strapping field in the transverse direction and \( h \) is the radial height above the photosphere. According to this definition, a larger value of the decay index indicates that the overlying field strength decreases faster. In practice, the field strengths at different heights can be obtained by extrapolating the coronal field assuming a potential field. A typical range of decay index \( n \) falls into 1.1 ~ 2.0 (Bateman 1978; Démodul & Aulanier 2010; Fan & Gibson 2007; Schrijver et al. 2008). Based on a sample of 10 events, Liu (2008, p. 1) found that “for a failed eruption, the field strength is about a factor of 3 stronger than that for a full eruption.” The decay index is usually measured along the polarity inversion line (PIL). In statistical studies such as Liu (2008), all the decay indices along a certain PIL are averaged to yield a single value representing the magnetic configuration of the corresponding active region. However, in some particular events, the decay index varies significantly along the PIL. Liu et al. (2010a) analyzed an eruptive event on 2005 January 15, in which a filament partially erupted. They found that the decay index above the region of the failed filament eruption was much smaller than those above eruptive regions. More recently, Guo et al. (2010) analyzed another failed event on 2005 May 27 and further confirmed that kink instability initiated this failed event, but that it was confined by the above strapping fields.

The main objective of this paper is to present a statistical study of the correlation between the decay index and CME speed. We collected 38 events and calculated the decay index of each event. A positive correlation between CME speed and decay index is found. In addition, we present analysis of a partial eruption on 2000 September 20 observed by the Big Bear Solar Observatory. Decay indices along the PIL are derived using...
Michelson Doppler Imager (MDI) magnetograms and different decay indices above the erupted/non-erupted region were found.

2. OBSERVATIONS AND MEASUREMENTS

In order to calculate the decay index, an extrapolation of the magnetic field is often used as coronal field measurement is not available. Nonlinear force free field (NLFFF) extrapolation of high-quality vector magnetograms is believed to represent the three-dimensional coronal magnetic field accurately. On the other hand, it is usually reasonable to assume that the strapping field may be more objectively described by potential fields, as fields turn potential above a certain height even in complicated active regions (Jing et al. 2008). In addition, the NLFFF method requires vector magnetograms with a large field of view (FOV), which were unavailable prior to the launch of the Helioseismic and Magnetic Imager on the Solar Dynamics Observatory (HMI/SDO). Therefore, the usage of potential field extrapolation that only requires that the line-of-sight magnetograms will expand the number of feasible events tremendously. Previous studies also suggest that the coronal field reconstructed assuming NLFFF may approach a potential configuration above an altitude of about 30 Mm (e.g., Jing et al. 2008). In this study, the potential field is computed using a Green’s function method (Chiu & Hilton 1977; Metcalf et al. 2008). The extrapolation was constructed by 100 grids in the vertical direction above the photosphere. The grid space is 1 pixel. With the MDI’s 1’98 pixel resolution, we are able to construct a three-dimensional magnetic field with a vertical dimension of about 140 Mm. In previous studies by Liu (2008) and Liu et al. (2010a), the strapping fields were believed to dominate in a range of 42–105 Mm. Xu et al. (2010) also found that a filament eruption mainly starts at 20 to 60 Mm using the stereoscopy method with EUV and Hα data. Therefore, in this study, decay indices are calculated in the same height range of 42–105 Mm as in the previous studies.

It is well known that filaments or flux ropes reside above the PILs which divide opposite magnetic polarity fluxes (Liu 2008). Therefore, the decay indices along the PIL in principle represent the majority of decay of the strapping field and were commonly calculated in previous analyses (Liu 2008; Guo et al. 2010). Typically, a PIL is identified by choosing the points with zero Gauss but large gradient on the magnetograms. However, in most of the events, the PIL extends far from the center of an active region or filament of interest, leading to substantial uncertainties in the averaged decay index along the entire PIL. Moreover, there are some sections of the PIL that belong to “quiet” regions that do not contribute to the initiation of eruption. Therefore, we choose to use the extent of a filament as a constraint to define an area within which the PIL is determined. The Sobel function (an embedded function of IDL) is then applied to a select area of the magnetogram and we find the PIL by looking for the pixels with the highest gradient and near-zero field strength.

As an example, we first present the process of calculating the decay index of the eruptive filament/CME event on 2002 September 29. This filament erupted around 22:20 UT and the corresponding CMEs were observed by LASCO at 23:54 UT. Graphical representations of the details are illustrated in Figure 1. The top left shows an Hα image of the filament prior to its eruption at 20:31 UT obtained from the Global Hα Network (GHN). The corresponding MDI magnetogram with the same FOV at 20:48 UT is shown in the top right panel. The PIL under the eruptive filament is plotted in white in the top right panel. In the middle panel, we plot log(Bt) versus log(h) for each pixel on the PIL. As mentioned, a height range of 42–105 Mm was used from extrapolated fields to calculate the decay index. In logarithm space, these values are converted to 3.73 and 4.65 as marked by the two vertical lines in the middle panel. Within such a height range, the derived decay indices are plotted in the bottom panel in ascending order of their values but regardless of their positions on the PIL. The lowest and highest values of the decay indices are 1.31 and 1.75, respectively. The mean decay index with 1σ uncertainty is 1.53 ± 0.11. Note that this event occurred in the quiet Sun. Not surprisingly, we will see in the next section that this decay index is relatively small compared with those of active regions.

3. STATISTICAL STUDY OF THE RELATIONSHIP BETWEEN DECAY INDICES AND CME SPEED

Motivated by the above analysis and previous studies (e.g., Liu 2008; Liu et al. 2010a), in this paper, we choose to compare the decay index with eruption kinematics, in particular, the linear speed of CMEs. As listed in Table 1, 38 events are selected for analysis. To minimize the projection effect on magnetic field extrapolation, only events not close to the solar limb (less than 60° from the disk center in both E–W and N–S directions) were selected. Note that not all of these events are associated with filament eruptions. According to Jing et al. (2004), some CMEs were associated with flares but no filaments were involved in the eruptions. In some cases, the absence of filament eruption might be simply due to the data gap, or because the material confined in filament channels is not dense enough to be observed as filaments (Martin 2000). In such cases, the magnetic configuration does not need to be different from that of events with filament eruptions. On the other hand, a number of eruptive filaments located in the quiet Sun do not incur detectable flares in X-ray emission. For those events without clearly observed filaments in Hα or EUV 304, flare ribbons are used to outline the center of the energy release area and the PIL is confined to such an area. In Table 1,1 decay indices of 38 events are listed, as well as the linear CME velocities obtained from the LASCO C2 catalog (http://cdaw.gsfc.nasa.gov/CME_list/index.html). For each event, the decay index is averaged in the height range of 42–105 Mm. As we can see in Figure 1, normally the decay index does not change too much within such a height range and the averaged value is pretty reasonable to present the magnetic gradient along the PIL.

The data points of these 38 events are presented in Figure 2 and fitted with a third-order polynomial function (\(y = a + bx + cx^2 + dx^3\)). Two distinct trends are found for the CME speed as a function of the decay index: (1) below about 1000 km s\(^{-1}\), CME speed increases steadily with decay index and (2) for CMEs with a speed above 1000 km s\(^{-1}\), the decay indices are almost constant at 2.2. This upper limit is consistent with the theoretical prediction of 2.0 (Kliem & Török 2006) and the result of 2.25 from observational study (Liu et al. 2008). In five events, the erupted filaments lay above quiet Sun regions and their decay indices are among the smallest, from 0.98 to 1.68. In Figure 2, these events are plotted with triangles. We are not able to draw any statistical conclusion using only five points, but these events appear to have relatively small decay indices, indicating that

1 Some events were not associated with detectable flare emission in X-rays. The listed “flare time” is actually the time for Hα emission or filament eruption.
4. A CASE STUDY OF AN ASYMMETRIC ERUPTION

Besides the fully eruptive events, partial and failed eruptions have attracted attention in recent years. The first failed eruption was studied by Ji et al. (2003). This event can be explained using the theory of kink instability and a strong strapping field as simulated well by Török & Kliem (2005).

A partial filament eruption on 2000 September 12, accompanied by an M1.0 flare and CME, is also of great interest. Wang et al. (2003) analyzed this event with multi-wavelength observations taken by the GHN, the Extreme ultraviolet Imaging Telescope, and LASCO. The authors tracked the erupting filament to about 20 solar radii. In the present study, we revisit this event with a focus on the spatial distribution of the decay index along the PIL. Using the line-of-sight magnetogram from MDI, we identified the PIL underlying the Hα filament before the eruption, as shown in the left panel of Figure 3. The small shift between the filament and the PIL is due to the projection effect. The PIL is color-coded according to the values of the decay index, and the mean decay index over the entire PIL is about 1.64. The white circle marks the non-erupting part of the filament.
A visual inspection immediately reveals that the non-erupting part generally has a smaller decay index than the erupting part. Panel (b) shows some samples of potential field lines superimposed on the line-of-sight MDI magnetogram and six given positions along the PIL. We then quantitatively examine the values of the decay index at these six positions. The decay indices are consistent with the theoretical expectation that a slow decay rate of the strapping field contributes more to confining the eruption while a quick decay of the strapping field puts less constraint on the eruption.

5. DISCUSSION

In this paper, we have analyzed 38 events that occurred away from the solar limb. The decay index of each event was calculated using the potential fields extrapolated from line-of-sight magnetograms. Combined with the linear velocities of CMEs obtained from the LASCO CME catalog, a good correlation is found. We noticed that the decay index increases steadily with CME speed up to 1000 km s\(^{-1}\). For faster CMEs, the decay index tends to have no significant change. The upper limit of the decay index is around 2.2, found by a polynomial fit to the data points. Our observational results are consistent with the modeling of Török & Kliem (2007). In principle, the dynamics of an eruption may be affected by an initiation force (\(F_i\)) to accelerate the erupting materials and a confined force (\(F_c\)) due to the strapping field. Consequently, the kinetic energy of a CME is

\[
\frac{1}{2}mv^2 = \int (F_i - F_c) dh,
\]

i.e.,

\[
v = \sqrt{\frac{2\int (F_i - F_c) dh}{m}},
\]

in which \(m\) is the mass of erupting materials, \(v\) is the CME speed, and \(h\) is the height. When the strapping fields decay very fast, i.e., have large decay indices, \(F_c\) is essentially zero. From the equations above, we can see that the CME speed is no longer correlated with the decay index. This scenario is
consistent with the flattened component of the curve plotted in Figure 2, in which the decay indices are around 2.2 while the CME speed spreads in a wide range from 1000 km s\(^{-1}\) to more than 3000 km s\(^{-1}\). Let us consider another case where the strapping field dominates due to a very slow decay (small decay index) in which we have \(\int (F_s) dh \geq \int (F_i) dh\), within a certain height range (for instance, from 42 Mm to 105 Mm).

Consequently, no filament could erupt under the constraint of such a magnetic configuration. From previous numerical simulations, (e.g., Démoulin & Aulanier 2010), the lower limit of the decay index could be 1.1 for the failed eruption. Our fitted plot in Figure 2 indicates that at a decay index equal to 1.0, the CME speed approaches zero. Above this threshold, the speed of the CME is proportional to the square root of the net resistance force of \(\Delta F = F_i - F_s\). According to the definition, the decay index \(n = -d \log(B_i)/d \log(h)\). The negative sign in logarithm space indicates that \(n\) is inversely proportional to the magnetic field strength and hence the restoring force, which in our case is \(F_s\). We can define \(F_i = (A/\sqrt{f(n)})\) and therefore Equation (2) becomes

\[
v = \sqrt{\frac{2}{m} \left[ \int F_i dh - \int \left(\frac{A}{\sqrt{f(n)}}\right) dh \right]},
\]

in which \(f(n)\) is a function that relates \(n\) and the force \(F_i, A\) is a coefficient related to the magnetic tension. Equation (3) in principle resembles the curvature component (with a CME speed less than 1000 km s\(^{-1}\)) of the plot in Figure 2. We note that an exact fitting to this equation is not available due to the lack of knowledge of the total mass of the CME, the magnetic tension coefficient of \(A\), and the exact form of \(f(n)\). However, this equation reveals the relationship between the decay index and CME dynamics with moderate speeds.

In addition, the case study of the asymmetric distribution of the decay index of the event on 2000 September 12 provides a physical picture that the relatively high decay index indicates weaker magnetic confinement in the strapping field. The filament component of the failed eruption was associated with a lower decay index representing a highly confined overlying arcade field. This result is consistent with that of Liu et al. (2010a).

Finally, we give the limitations of our study. We note that only one magnetogram prior, usually 2–3 hr, to each eruption is used for extrapolation. Any rapid change of magnetic field, such as a flux emergence, is not considered during this time period before eruptions. A more detailed analysis with high cadence magnetograms, such as observations by SDO/HMI, will provide...
more accurate measurements of the decay index. The results from potential field extrapolation need to be compared with those from other extrapolation methods, such as NLFFF. We used a height range of 42–105 Mm as was commonly used in previous studies (Liu 2008; Liu et al. 2010b). But different height selections could affect the calculation of the decay index because the exact height ranges of strapping fields vary from one event to another. The filament height, if it can be measured accurately, may provide an important hint in solving this problem. In addition, a sophisticated PIL selection tool can improve the accuracy of decay index measurements.

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