An investigation of the applicability of SPIV for the analysis of the dynamics of floating offshore wind platforms

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Abstract

There is a need for new numerical tools to capture the physics of floating wind platforms more accurately to refine engineering designs and reduce costs. The conventional measurements apparatus in tank tests, including wave probes, velocity and current profilers, as well as doppler sensors, are unable to give a full 3D picture of velocity, pressure, and turbulence. In tank testing, the use of the underwater stereoscopic PIV method to fully characterise the 3D flow field around floating platforms can provide a rich source of validation data and overcome some of the limitations associated with more classical measurement techniques. This optical technique can be used to accurately measure the random and chaotic structure of turbulent flows around the floater. Moreover, the main characteristics of turbulence of the flow around the floater, such as rotationality, diffusivity, irregularity, as well as dissipation, can be extracted and studied. The underwater S-PIV method has been widely used for marine and offshore applications, including studies on ship and propeller wakes and tidal stream turbines; however, to date, this technology has not seen widespread use for the hydrodynamic study of floating offshore wind turbines. Therefore, in the current study, the key considerations for using S-PIV for this purpose are discussed; meanwhile, the related studies in the field of quantitative flow measurements are reviewed.

Keywords: Floating offshore wind turbine, Stereoscopic particle Image velocimetry, SPIV, experimental campaign, tank testing, measurement techniques
Introduction

Considering the 30 MW Hywind Scotland, the 24 MW WindFloat project in Portugal and upcoming projects including 30 MW EFGL in France and 88 MW Hywind Tampen (WindEurope, 2020), Europe is on course to become a world leader in floating offshore wind. Current estimations for floating offshore wind turbines (FOWTs) suggest that the cost of energy will fall by 70% and reach 40 Eur/MWh by 2050, while total installed capacity is expected to increase to 250 GW (DNV GL, 2020). However, these cost reductions are not guaranteed and will require robust design tools to enable designers to balance cost reduction, structural integrity, and project risk. A wide variety of engineering design tools with a limited representation of the underlying physics have been developed and employed for FOWT design (Cordle and Jonkman, 2011). A comprehensive review of the current state of the art of numerical tools in the field of FOWTs was carried out in press (Otter et al., 2021).

These numerical codes are based on either the frequency or time domains analysis. As low fidelity models, the frequency-domain codes utilise strip theory, panel method, or a combination of both. While this approach provides shorter CPU time, a limited capacity to capture the low-frequency motion of the floating platform result in inconsistencies and error. These errors could be up to a 20% difference in the mean value of the results (Rahimi et al., 2016). Conversely, time-domain codes, including full Computations Fluid Dynamics (CFD) simulations, provide a more complete picture of platform responses as nonlinearity is considered. Such CFD codes provide high fidelity data such as turbulent kinetic energy, velocity distribution, flow wakes, as well as the wave-making characteristics of floater (Liu et al., 2017). Accurately capturing turbulence modelling is essential for response analysis of the floater so that the engineers can produce reliable and cost-effective designs in terms of fatigue load estimation and structural and mooring design of FOWTs.

In CFD, turbulence modelling involves a mathematical model that estimates the effects of turbulence on fluid flow. Although there is no analytical theory to predict turbulent flows, many researchers have numerically studied turbulence formation, and several hybrid models have been developed. A review on the state of the art of hybrid turbulence models is conducted by (Chaouat, 2017). In respect of turbulence modelling, the CFD codes provide high fidelity data, such as Reynolds stresses, specific dissipation rate (SDR), turbulent kinetic energy (TKE), along with TKE production and dissipation rate (TDR). Standard turbulence models for these numerical codes are
Spalart–Allmaras, $k-\varepsilon$, $k-\omega$, $SST$, and RSM. Alongside, some researchers favour the use of LES approach to fully simulating the turbulent structures of the flow. These high-fidelity numerical approaches have a significant computational expense compared to linearised engineering models however, there use will is required to resolved detailed flow phenomenon and system response. There is a requirement for validation data to reduce inaccuracies and errors in these high-fidelity numerical simulations. A study on the accuracy of turbulence models was undertaken by (Rezaeiha et al., 2019), which reveals that uncertainty levels for demonstration of a model’s wake in fluid flow could reach 30% near the wall of the model.

In both frequency and time domain approaches, there is a lack of accurate verification data. As the technologies advance, high fidelity models will see greater adoption. Moreover, the validation of these advanced models will be critical. Tank testing and real-world demonstrations are sources of validation data, though higher accuracy measurement apparatus is required to fully resolve flows and response. In tank tests, the single-point wave measurement equipment includes wave probes, laser doppler velocimeters (LDV), as well as acoustic doppler velocimeters (ADV). Additionally, for current measurements, there are velocity profilers such as Acoustic Doppler Current Profiler (ADCP), as well as hot wires or pitot tubes. These are practical tools to measure fluid velocity only at individual points in the tank. Moreover, these pieces of experimental equipment have their associated errors; a comprehensive review of underwater speedometer equipment and its measurements error is conducted by (Fuentes-Pérez et al., 2018). Using only these instruments, it is impossible to fully and accurately understand the tank’s flow regime, for instance, full velocity and pressure distribution contour; and so, a complete 3D picture of the fluid flow cannot be produced for the validation of high-fidelity numerical models.

Comprehensive flow characterisation can be achieved by stereoscopic particle image velocimetry (S-PIV). The S-PIV is an optical measurement technique where the velocity field of an entire region within the flow is measured simultaneously. This is the fundamental advantage of S-PIV against single point measurement methods. S-PIV facilitates both the extraction of measurement data and the visualisation of flow structures. An optical non-intrusive technique allows a complete picture of the turbulent flow field to be produced; it reveals insights about the study

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1 $K$-epsilon
2 $K$-omega
3 Menter’s Shear Stress Transport
4 Reynolds stress equation model
5 Large Eddy simulation
domain, for instance, velocity, turbulent kinetic energy, and vorticity distribution. Moreover, as a high-fidelity method, the resolution of data captured by S-PIV is equivalent to several thousand measuring points in an assumed interrogation window (See Figure 1). Therefore, in an assumed spatial volume, the fluid flow parameters can be measured with high resolution.

Figure 1 Reconstruction procedure of 3D-3C flow with multiple 2D-3C SPIV velocity planes: a) Interested area at the model aft; b) Locations of multiple-2D scanning SPIV planes; c) Reconstructed 3D volume; d) 3 Component flow field in 2D planes; e) 3D component flow field (Wu et al., 2020)

The S-PIV technique is widely used for studying the aerodynamics of offshore wind turbines (Figure 2), e.g. (Bayati et al., 2018), (Xiao et al., 2011), (Wang et al., 2015) and for the validation of complementary CFD simulations (Desmond et al., 2014). Additionally, some researchers use the S-PIV technique to study other marine renewable technologies (Day et al., 2015); however, the use of underwater S-PIV for FOWT’s tank testing is an emerging field. This method can be used to fully characterise the 3D flow field around floating platforms in the laboratory environment, provide a rich source of validation data and overcome some of the limitations associated with conventional measuring equipment of fluid flow (Chen et al., 2020).
This technique has not seen widespread use in FOWT tank test campaigns to date. This paper reviews state of the art in S-PIV techniques and identifies opportunities for their use in tank test campaigns to better understand the flows around the floater and to provide a rich source of validation data for advanced numerical models. Despite the high-resolution results of S-PIV, there are uncertainties associated with the laser frequency, tracer particle response, and hardware synchronisation in each test case. Therefore, to utilise this technology for the hydrodynamics of FOWTs, there are various errors, uncertainties, and quantitative parameters to be studied. This review paper covers the vast majority of these parameters in the following section and discusses the relevant research in the field of quantitative flow visualisation.

2 The S-PIV, its application, and challenges for FOWT tank testing

2.1 Theory of Particle Image Velocimetry

The basis of PIV is the measurement of particles’ displacement at different time steps. The fluid flow is filled with traceable particles; then, a laser light passed through a lens becomes a flat light sheet and illuminates these particles. The PIV measurement is achieved by group tracking of fluid particles and processing their trajectory at different time intervals. By high-frame imaging of the illuminated particles and post-processing of consecutive images, the particle group’s displacement is extracted for each time step, and their relative velocities are calculated using a group distance and a sample time (See Figure 3). This travelling distance depends on parameters such as flow rate,
camera frame rate, as well as the level of fluid flow turbulence. Since this method is an indirect measurement, the movement of tracer particles within the fluid flow is examined instead of determining the flow attributes. Therefore, the type of particle seeds and their properties are chosen based on the studied fluid and turbulence.

**Figure 3 Schematic description of the PIV principle** (Ismadi et al., 2013)

Various methods such as Gaussian, phase discrimination and Dynamic Mean Value Operator have been developed to review and post-process the PIV raw data (Markus, Raffel, Christian E. Willert, Fulvio Scarano, 2018). These image comparison methods can later be distinguished from each other in their local or global regularisation schemes. Global schemes iteratively optimise the entire flow field and its displacement path, while in the local methods, a number of interrogation windows are selected, and the group path of particles inside these windows are investigated in the consecutive images (See Figure 4). This iterative phase is repeated for all captured images in the interrogation windows. A well-known approach to conduct this iterative step is to use the cross-correlation method. The cross-correlation method is used commonly in particle image velocimetry.
Figure 4 Two frames cross-correlation PIV (Choi et al., 2011)

A review of the theory of the cross-correlation method and its application in particle image velocimetry has been conducted by (Keane and Adrian, 1992). Based on this method, if the parameter $D$ is considered the constant displacement of all particles in an interrogation window, then particle locations at the next time step are given by Equation (1).

\[
X_i' = X_i + D = \begin{pmatrix} x_i + D_x \\ y_i + D_y \\ z_i + D_z \end{pmatrix}
\]

Moreover, by assuming the particle image displacement given by Equation (2), the image intensity for the second step is calculated from Equation (3).

\[
d = \begin{pmatrix} M \cdot D_x \\ M \cdot D_y \\ M \cdot D_z \end{pmatrix}
\]

\[
I'(x, \Gamma) = \sum_{j=1}^{n} V_0'(X_j + D) \tau(x - x_j - d),
\]

where $V_0'(X)$ defines the interrogation volume during the second time step (see Figure 5).
If the light sheet and the windowing characteristic are assumed identical for images in two consecutive time steps, the cross-correlation function of the interrogation area can be written as:

\[ R_{ij}(s, \Gamma, D) = \sum_{i,j} V_0(X_j) V_0(X_j + D) R_i(x_i + x_j + s - d), \]

(4)

Where \( V_0 \) is the interrogation volume, and \( s = (x, y) \), \( s_D = M \cdot (\Delta x, \Delta y) \) is the particle tracer displacement on the image. The \( i \neq j \) terms represent the correlation of different randomly distributed particles, so, they are mainly the noise in the correlation plane. Moreover, the \( i = j \) terms are the desired displacement information. With distinguishing the noise from the desired displacement information, the cross correlation function is given by Equation (5).

\[ R_{ii}(s, \Gamma, D) = \sum_{i,j} V_0(X_j) V_0(X_j + D) R_i(x_i + x_j + s - d) \]

\[ + R_i(s - d) \sum_{i=1}^{N} V_0(X_j) V_0(X_j + D) \]

(5)

Therefore, the component of the cross-correlation function correspond to particle image is as (6).

\[ R_D(s, \Gamma, D) = R_i(s - d) \sum_{i=1}^{N} V_0(X_j) V_0(X_j + D) \]

(6)
Hence for a given number of particles inside an interrogation window, the maximum displacement correlation peak that can be reached is at $s = d$ (see Figure 6). The location of this correlation peak is representative of the maximum particles group displacement. The cross-correlation method enables us to locate the particles groups in each time step; so that having the time step and particles group displacement results in having the velocity vectors and contours.

2.2 State of the art of Particle Image Velocimetry in tank tests

PIV was first used for tank testing by Dong (Dong et al., 1997). The main motivation of this research was to wave structure near the bow of a ship model. The test was performed using a camera and an underwater light sheet. After processing the data, the researchers extracted a two-dimensional velocity field for a 3.05 m ship model in flow with a Froude number in the range of 0.17 to 0.45. These measurements also determined the velocity near the free surface. In this research, a special focus was on flow vorticity production and its energy losses. This result was significant as the PIV method revealed the turbulence intensity and the 3D velocity distribution in the tank test campaign (see Figure 7).
Another study was performed by Tukker et al. (Tukker et al., 2000). The motivation of the research was to study the feasibility of using the PIV technique to measure the unsteady spatial structure of flow in test tanks. Attention was paid to the main features of PIV in test tanks, including the seeding of a large quantity of water, the visibility of the particle in water, as well as measuring the accuracy of the method. For the first time, a digital camera was used for PIV in a test tank. A 64x64 pixels interrogation window was used to record the wake area behind a passing ship model. The PIV equipment was stationary, which limited the study to examining only one area of the ship’s path. However, the study result was beneficial since it could visualise the unsteady and spatial flow dynamics around a model. Tukker’s study shows that using a higher-resolution digital camera increases the frame accuracy and quality of data for the two-dimensional plane. Using this method in a tank test was promising since it could record the instantaneous flow velocity measurements. However, the use of 2D PIV causes out off-plane velocity error, which is the calculation errors for the velocity vectors in the third dimension normal to the light sheet.

In the research described above, all PIV experiments only recorded two-dimensional velocity vectors, and the error in the third dimension was due because of the particles leaving the thin light sheet. This error in the third dimension is known as the ubiquity problem. This is a disadvantage since the flow structure after the model has a significant 3D characteristic. In the single-camera method, the particle velocity can be calculated correctly only in two dimensions on the laser screen. In the S-PIV method, the particle velocity in the third dimension can also be obtained by post-processing of vectors (Baghaie, 2019). Therefore, by having the corresponding images recorded
by the two cameras, the actual velocity vector in the third dimension can be calculated with a geometric reconstruction (see Figure 8).

Figure 8 Comparing PIV and S-PIV technique to solve the ubiquity problem for the out of plane vectors (Jux et al., 2018)

An important parameter in the S-PIV test is the angle of cameras relative to the light sheet. Lee et al. conducted a sensitivity analysis (Lee et al., 2014) for different camera angles in the S-PIV method. They extracted the maximum value of error related to in-plane and out-of-plane velocity vectors for different cameras angles (see Figure 9). The research shows that the ideal camera angles are symmetric 45 degrees to the light sheet, which may not be suitable for all test campaigns depending on the dimensions of the model and the dimensions of the basin or the cameras’ distance to the illuminated plane.

Figure 9 symmetric and asymmetric camera angle in an S-PIV test (Lee et al., 2014)
Research was conducted on various types of S-PIV systems with different arrangements consisting of two vertical cylinders (Egeberg et al., 2014). The purpose of the experiment was to study the generated vortex of a 3.047 m ship model. The new design allowed for the capture of vortices with a frequency of 3 Hz. The distribution of velocity and vorticity are used to characterise vortices. Since the PIV method can capture and visualise the instantaneous velocity and vorticity field, the vortex in the fluid flow can be captured simultaneously. Having an accurate estimation of vortex around the model can improve the design to reduce undesired phenomena such as vortex-induced vibration and motion (VIV, VIM), multi-body flow interaction, wave-current body interaction, sloshing, as well as the instantaneous position of wave load. Additionally, this estimation can lead to a better understanding of flow wake around the floater model, which leads to an accurate estimation of floater motion in different environmental conditions.

S-PIV equipment is widely used in marine engineering applications since it can provide high fidelity results of applied force on the model. Lee et al. examine the wave field of a containership model (Lee et al., 2009). Their velocimetry measurements were at four different sections of the model, using CCD cameras\(^1\) with a resolution of 1024x1024 pixels. Utilising the S-PIV technique enabled the extraction of velocity and vorticity distributions to capture phenomena such as counter-rotating vortices in the model’s wake area. The result of this study characterised the near-wake region for the model. Different counter-rotating longitudinal vortices, their location, as well as their trajectories were also determined. Another achievement of this S-PIV-based experimental campaign was finding the vortex’s centre in different loading conditions. This facilitates an examination of the inflow condition and a clear picture of the turbulent intensity distribution and its vortexes in the wake area of the model (see Figure 10).

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\(^1\) Charge-coupled device camera (Anthony F. Molland, 2008)
S-PIV is a suitable tool for studying turbulence flows; however, it is critical to limit the uncertainty of the method in test campaigns. Yoon et al. carried out a benchmarking investigation by examining a ship model with a length of 3.048 m using the S-PIV system. The first aim of the research was to create a manoeuvre database for that model (Yoon et al., 2015). The second aim was to develop a systematic method for examining the S-PIV uncertainties, setting the validity criteria on converging error and performing a standard uncertainty assessment. The test campaign was carried out for pure yaw and sway tests. Moreover, the result included the axial velocity and turbulent kinetic energy at the measurement sections (See Figure 11). The convergence error of their test campaign was less than 1% of the towed velocity $U_c$ for the velocity distribution field. Additionally, their standard uncertainty was in the range of 2-3% $U_c$ for the velocity fields.
In the underwater S-PIV technique, the equipment, including cameras and laser, are kept underwater. These attachments may influence the flow regime by causing backflow and interaction with the flow around the model. This issue is examined by Han et al., who investigated the uncertainties of the S-PIV method for its application in the tank test (Han et al., 2018). A ship model with a Froude scale of 1/100 in both uniform flow and nominal wake flow was studied. Two 14 Hz digital cameras were used to undertake the detailed examination. In order to quantitatively assess the high fidelity results, the proposed procedure of ITTC (ITTC, 2008) and the proposed method of Yoon’s research (Yoon et al., 2015) was utilised. In their experiment, it was found that the torpedo configuration of the S-PIV system does not significantly affect the computational velocity field and the resulting error was negligible. The nominal wakefield measured in that research is shown in Figure 12. The research showed that data obtained with the S-PIV technique are both accurate and high resolution. Moreover, the equipment in this technique does not interfere with the fluid flow.

| a | b | c |
|---|---|---|
| ![Axial velocity](image1) | ![Cross-plan VW-vectors](image2) | ![Turbulent kinetic energy](image3) |

Figure 11 Pure yaw test: a. Axial velocity, b. cross-plan VW-vectors, c. turbulent kinetic energy (Yoon et al., 2015)
To date, the use of underwater S-PIV in tank tests has been limited to the study of ship propellers (Go et al., 2019), tidal stream turbines (Seo et al., 2016), the ship model wave field (Mallat et al., 2015), (Jacobi et al., 2016), (Tukker et al., 2000) and basic phenomena such as vortex-induced vibrations (Ashworth Briggs et al., 2019). There are successful attempts in the literature to use this technology to create a high-fidelity ship manoeuvring database (Yoon et al., 2015). The same approach can be used for the hydrodynamic study of FOWT with regard to minimising the uncertainty of velocity measurements in the test campaign. The high-resolution data of vorticity, full velocity distribution and turbulent kinetic energy then can be used as a source of validation data for numerical codes for FOWTs.
3 Critical parameters of underwater S-PIV

The most critical issues in using S-PIV underwater and in the wave-basin are the type of seeding particles, out-of-plane velocity of particles, illumination in water, imaging technique, different camera angles and the associated uncertainties. These critical parameters are discussed in this section.

The study area in the tank test usually has a significant three-dimensional turbulent characteristic. Many parameters such as image pixel size, particle strength and density, velocity gradients, turbulence variation, and noise level (Scharnowski and Kähler, 2016) are involved in error generation and raising the uncertainty of this method. In the previous two decades, researchers have tried to identify and reduce these errors sources (Sciacchitano, 2019), (Markus, Raffel, Christian E. Willert, Fulvio Scarano, 2018), (Kähler et al., 2012), (Charonko and Vlachos, 2013), (Bhattacharya et al., 2018), (Neal et al., 2015). One of the well-known methods is uncertainty surface (Timmins et al., 2012), in which captured images are analysed for parameters affecting the error.

3.1 Particle seeds

The S-PIV technique is an indirect approach, so instead of directly examining the flow, the response of illuminated particles in the flow is analysed. Therefore, in particle selection, the particle mass and the optical reflectance are important. In seeding selection, other factors such as the distribution of particles and the seeding density in the fluid should also be studied for each test; these criteria have been well studied in (Markus, Raffel. Christian E. Willert, Fulvio Scarano, 2018).

The primary sources of error are the effect of gravity and buoyancy on the motion and response of particles. Particles with lower density than the fluid follow the fluid path very well (See Figure 13). However, the cumulative effect collisions between particles and the fluid vortex cause unwanted random movement of the particles. This random motion is called Brownian motion (Olsen and Adrian, 2000), leading to measurement error up to 15% of fluid flow velocity (Catipovic et al., 2013). Contrarily, coarse particles with a density higher than fluid do not respond well to fluid flow turbulence (Al-Muhammad et al., 2018).

The reflectivity of the particles is another topic of interest. Coated glass particles are commonly used in underwater PIV testing. Their uniform dimensions and excellent reflectivity attributes made them suitable for underwater application. However, in typical wave basins (Desmond et al., 2016), the need for high quantities of particles for several tests makes the coated glass an uneconomical option.
Figure 13 Trajectories of vortices, A. course seeding $Ek = 1 \times 10^{-4}$ B. dense seeding $Ek = 7 \times 10^{-6}$ (Chong et al., 2020)

Fluorescent particles can also be used, as they avoid unwanted reflection of the model surface and bubbles. However, these particles are expensive. A suitable alternative is Orgasol and Vestosint particles (Schröder et al., 2020), which have the same reflectance quality and good economical efficiency. Ashworth Briggs et al. have recently proposed a practical alternative to these conventional particles during their test campaigns (Ashworth Briggs et al., 2019). In that research, a series of fluorescent particles with 57 mm mean diameter were fabricated and coloured with Rhodamine 6G. In this research the uncertainty of the experiment is reduced to 0.5 mm. In particle selection, other factors such as the distribution of particles and the seeding density in the fluid should also be studied for each test; these criteria have been well studied in (Markus, Raffel. Christian E. Willert, Fulvio Scarano, 2018). Nonetheless, choosing the right particles are based on test condition and the understudied phenomenon.

### 3.2 Illumination

Lasers are one of the integral components of PIV tests. These elements create monochromatic light with high energy density. Passing this light through an optic lens turns it into a thin light sheet (See Figure 14), which illuminates the particles. In comparison with aerodynamics, in hydrodynamics, the fluid is denser, and it is necessary to use high power lasers for illumination. For the first PIV experiments, a 20 MJ laser was used in the tank test described by (Dong et al., 1997); more recently, ND YAG lasers provide illumination power up to 200 MJ at a wavelength
of 532 nm (Abdulwahab et al., 2020). At this maximum energy, the maximum repetition frequency is within the range of 7-25 Hz.

The laser frequency must be synchronised with the camera shooting frequency, and the repetition rate of the laser radiation should be adjusted according to the imaging rate (Jacobi et al., 2016). For example, a laser with a power of 200 MJ has an approximate repetition frequency of 20 Hz; if a higher frequency is needed, the laser power should be decreased. However, this results in less illumination in the water medium and lower image quality.

![Figure 14 Stereo-PIV system in a towing tank](Jacobi et al., 2016)

Another issue is the high reflection from the model surface in the water environment (see Figure 15), which is due to the high laser illumination. Reflection problems at or near the model wall boundary due to high laser illumination can lead to errors and has been examined in various studies. Sciacchitano investigated the reduction of errors in this area as well as the overall reduction of method uncertainty (Sciacchitano, 2019). A comprehensive methodology for studying this error and introducing approaches to prevent it in a PIV campaign is given by (Adrian et al., 2011). A possible solution to this issue is to paint the model black or fabricate the model using acrylic material. However, it is not possible to made complex models out of these materials.
In the PIV method, the velocity components are usually calculated on a two-dimensional light sheet. Using only one camera results in a perspective error as any out of the plane movement of particles leads to an error in calculating the third-dimension vectors (Ajay K. Prasad, 2000). This error is reduced using the S-PIV method (two cameras), although the accuracy of the results may still be affected since the technique is based on 2D assumption, and any particle motion vector outside the particle plane affect the results.

Several particles that move across the illuminated light-sheet could affect the light sheet’s intensity in different images. The particles disappear when leaving the light sheet, and the new particles are replaced constantly; this affect the post-processing schemes’ error (Wieneke, 2017). This random error is one of the fundamental and dominant errors in the S-PIV method. A recommended approach to mitigate this error is to ensure that less than a quarter of the particles leave the light sheet between each two laser pulses (Adrian et al., 2011).

In order to limit out of plane loss, (Markus, Raffel, Christian E. Willert, Fulvio Scarano, 2018) propose several methods for recording particle path; however, each of these methods has its own advantages and disadvantages. One approach is to divide the time interval between pulses. The velocity is obtained by reconstructing the movements in a time interval (Zhong Li, Jinwei Ye, Yu Ji, Hao Sheng, 2019). Therefore, this method reduces the fluctuations of the constructed velocity field both in the third dimension and on the light sheet plan.

**Figure 15 Reflection issue because of high illumination** (Grizzi et al., 2010)
3.3 CCD cameras and image processing

The advantage of the S-PIV over the PIV method is using two digital cameras instead of one camera; thus, the third velocity vector is calculated correctly with a geometrical reconstruction of images, and the associated error is reduced. However, the presence of two cameras with different angles leads to a loss of a part of the interrogation window. Moreover, the lenses’ angle and the requirement for a mapping technique results in a relative error in the overall calculation of the velocity field.

Various arrangements for the two cameras have been suggested by (Markus, Raffel. Christian E. Willert, Fulvio Scarano, 2018). However, a 45-degree angle is an optimal angle in terms of error reduction to error ratio of 1 percent (Lee et al., 2014). Jurgens et al. have also investigated this issue in their study (Jurgens, 2007) and proposed a symmetrical setup for two cameras to reduce the error. Although this type of arrangement usually has the least error for the third velocity vector, it strongly affects the vector and fluid distribution around the model. In any case, the dimensions of the model, tank test, and the interrogation window are the three primary parameters that set the distance and angle of the cameras to the light sheet.

After capturing the raw image data, there are a significant number of outliers, and the raw data needs to be pre-processed. Image processing in the S-PIV method usually has three main phases (Garcia, 2011): (1) Data validation and velocity vectors (outliners) extraction, (2) Replacement scheme, and (3) Data assimilation. A comprehensive review of many of these pre-processing algorithms’ advantages and disadvantages has been carried out by (Westerweel et al., 2013). Many researchers have worked on optimising these algorithms (Liu et al., 2008); however, one of the most valid methods for this purpose is the global histogram filter (Pun et al., 2007).

Researchers have worked on developing different schemes to investigate the uncertainty of S-PIV and the parameters that have the greatest impact on uncertainty. Among the well-known and widely used methods, we can mention the uncertainty surface method (Timmins et al., 2012), multi-pulse and multi-frame (Westerweel et al., 2013), particle disparity (Sciacchitano, 2019), and peak ratio method (Charonko and Vlachos, 2013). These schemes and their governing mathematical equations have been thoroughly discussed and reviewed in (Sciacchitano, 2019), (Markus, Raffel. Christian E. Willert, Fulvio Scarano, 2018), (Wieneke, 2017), (Adrian, R. J. and Westerweel, 2011).
4 Application of underwater S-PIV for tank testing of FOWTs

There is a variety of hydrodynamical phenomena that can be studied with underwater SPIV. The main contribution of this technique is in the field of wave kinematics, viscousity study, as well as the characteristics of the turbulence in the flow around the floaters. Hydrodynamical phenomena related to floater design and their degree of importance are outlined in Table 1, which are based on studies in the OC5 project (Robertson et al., 2017), (Amy Robertson, n.d.).

Table 1 The hydrodynamical phenomenon ident. ranking based on OC5 project (H: High, M: Medium, L: Low)

| Row | Phenomena                          | Importance | Physics Understanding | Validation Needs | Suitability of underwater S-PIV for providing validation data |
|-----|------------------------------------|------------|-----------------------|------------------|-------------------------------------------------------------|
| 1   | VIV/VIM - substructure             | M          | L                     | H                | Yes                                                         |
| 2   | Nonlinear excitation – diff/sum/mean | H          | M                     | H                | Yes                                                         |
| 3   | Short-crested waves                | M          | H                     | H                | Yes                                                         |
| 4   | Marine growth influence on loads   | L          | H                     | H                | Yes                                                         |
| 5   | Breaking/steep wave loads          | L          | M                     | H                | Yes                                                         |
| 6   | Wave-current body interaction      | H          | M                     | M                | Yes                                                         |
| 7   | Viscous load model                 | H          | M                     | H                | Yes                                                         |
| 8   | Multi-body flow interaction        | H          | M                     | H                | Yes                                                         |

4.1 Vortex induced vibration and motion

One field of the S-PIV contribution to FOWTs design is to study the vorticity field behind the model. This could be beneficial to study problems such as vortex-induced vibrations and motions. An experimental of flow-induced oscillations of a floating model spar-type floater is conducted by Carlson (Carlson and Modarres-Sadeghi, 2018). The model was the 1:470 scale of Hywind spar platform. In this study, the amplitude and frequency of the platform response is captured by tracker cameras. Moreover, wake visualisation was carried out by snap shooting of smoke behind the model. Using S-PIV in this type of study could be beneficial since the vorticity core in Z direction (normal to the water surface) can be captured, and this can be done in for different shedding frequencies. Then, the trajectory of these vortexes and their excitation region can be identified. This valuable data can then be used to
minimising the VIV effect, as well as analysing different VIV suppression methods, for instance, for reviewing different strake shapes on the model.

4.2 Nonlinear wave loads

The S-PIV result could be used to study of the Nonlinear wave effects on the floater, as the linear wave assumption has considerable error for wave loading and the platform response estimation. Among the ongoing research, the conducted research by (Pan and Ishihara, 2018) can be mentioned. In this research, the effect of nonlinear assumption for motion analysing of FOWT with a Semisubmersible floater is reviewed. It is shown that compared to nonlinear waves, linear wave theory has an overestimation of 17.6% for pitch and 24.6% for heave responses of the platform.

A study on the effects of fully nonlinear wave loads on FOWTs is conducted in press (Xu et al., 2019). In this study the effect of linear and fully nonlinear wave loads on OC4 semi-submersible platform is examined. The focus of research was mainly on floater motion, structural responses, as well as mooring line tension due to nonlinear and linear waves. The parameter that takes into account was the wave free-surface location and velocity distribution near the platform. Other results that were study were included the wave spectrum at different frequency range. The S-PIV method can make a great contribution here, since it is an instantaneous and visual method, these results can be visualised and examined simultaneously.

Floating wind turbine is a complex system and the motion of the supporting platform, as well as the turbine performance are coupled. Having an appropriate understanding of nonlinear wave excitation on floater could be useful to estimate the wave loading on the floater, as well as floater responses in different sea state. This understanding can later be used to optimise the turbine control system. This optimal control system needs to have efficiency for disturbance rejection and load reduction on turbine. A review on the state of the art of the control strategy for FOWT is carried out by (Salic et al., 2019). Another note about FOWTs is the LCOE. From control point of view, the control system should operate turbine near its optimum operation point against different transient and steady state aero and hydrodynamic loading conditions. In realistic sea state, nonlinear waves cause critical floater responses in terms of critical floater motion, mooring responses, as well as wave elevation around the platform. Providing data with S-PIV to study on the nonlinear wave effect, as well as possible load cases, can later be use for designing reliable turbine controller systems, better turbine efficiency, and lower LCoE.
4.3 Short-crested waves

In comparison to slender members of Jacket platforms, the sub-structure of a FOWT is a large-scale bluff body. So that the presence of substructure in the incident waves, make scattered waves in the vicinity area. As a classical approach, the diffraction theory can use to study the hydrodynamics of these bluff body in waves. Moreover, boundary element method can use to solve this diffraction of waves. Diffraction theory is widely used for solving linear plane waves around hydrodynamically bluff body; the experimental validation for this method can find in literature (Chakrabarti and Tam, 1975). As discussed by (Hedges et al., 1993), although the diffraction theory is a practical approach to model wind generated waves, these waves are modelled more realistic with Short-crested waves. Application of short crested waves are the matter of interest for many researchers (Wang et al., 2019), (Wei and Dalrymple, 2017), (Vasarmidis et al., 2019).

Variety of study on short-crested waves is conducted in literature, one of which is the experimental study on directional hydrodynamic coefficient and wave force due to spreading angles of these waves (Ng et al., 2020). In this study the wave surface elevation, as well as force exerted on a cylinder model is studied. Range of 0 to 45 degrees is considered for directional spreading angles. Then, the relation of this parameter with Keulegan-Carpenter (KC) number is reviewed. Main result of this study is the wave time history, wave elevation, and wave force on the model, regarding the spreading angles. Drag and inertia coefficient is extracted. Moreover, the effect of short-crested waves on the wave force is studied. From the optical perspective, S-PIV can have an indirect contribution for study of short-crested waves. Although, this method can not be used for direct measurements of applied forces, as well as drag and inertia coefficient; the wave elevation and surface level change can be extracted in real time. Having the turbulent contours, velocity field and pressure field in this elevation studied, could easily help to identify the applied forces. Although, for studding the FOWT in wave tank, sensors such as Tri-axial accelerometer, Inertia motion unit, and different load cells are practical equipment. For the study of wave kinematics and dynamics, researchers can only use resistive wave gauges, current profiler, as well as Aquadopp, which are sampling the data in some point. The S-PIV can be useful to study the short-crested waves, as it brings instantaneous field contour relted to study wave kinematic.

4.4 Marine growth influence on loads

There are strong ways for S-PIV contribution to study Marine growth effect on FOWTs. Marine growth could have different effects on the substructure of FOWTs. It is mainly caused to increase the thickness, structural weigh, drag
coefficient, as well as hydrodynamical added mass of the platform. The effect of marine growth on dynamics of offshore wind support structures is studied by many researchers, from which the conducted research by (Martinez-Luengo et al., 2017) can be mentioned. In this research a special focus is set to the effect of zonation and thickness of marine growth on mode shapes, as well as natural and bucking frequencies of supporting platform. In order to estimate the wave force, drag and inertia coefficient are calculated only based on offshore standards and guidelines (DNV-OS-J101, 2014), (API 2A-WSD, 2014). The main variation of drag and inertia coefficient due to marine growth is related to thickness and distribution of the growth, Keulegan-Carpenter number, relative surface tension, along with direction of incident waves. The drag component integration can be conduct with S-PIV method.

This drag interrogation could be align with inflow, crossflow, as well as specific directions, for instance align with vortex drags. This result could be used to study marine growth effect on the floater drag coefficient with different feasible growth thickness and distribution. Since the result are based on quantitative optic measurement, it can also be used to study the turbulence and vortexes generation of marine growth on the floater.

The S-PIV experiments could be used to study the marine growth effect on tendon and mooring line responses. The marine growth has influence on the mooring lines and umbilical cables. This could happen by incising their diameter. Although in practice this thickness increase is considered as an ideal and homogeneous roughness, studies are shows that this idealisation is not valid for realistic condition in the sea. In realistic situation, a great portion of marine growth could be attached to specific potion of mooring lines. A research on effect of marine growth on FOWTs mooring lines is carried out in press (Pham et al., 2017); in which the dynamic behaviour of mooring lines under the effect of quantity and the distribution of marine growth is studied. In this research, different distribution of marine growth is considered, and for each test case, the tensions and effective tension in Anchor and Fairlead points is investigated. In literature (Chuang et al., 2021), conventional equipment such as load cells is mainly used to study the FOWT’s mooring line responses. However, the S-PIV can also have a contribution to this topic.

The point is that different materials can be used for FOWTs mooring, for lines, such as synthetic ropes, chains, and wire ropes. This material could have a different effect on marine growth, such as different intensities or distribution of growth on them. S-PIV could be utilised along with loadcells, so meanwhile that the tension in both failed and the anchor is provided, the main parameters of marine growth on a mooring can be examined in interrogation windows along the mooring length. These turbulent parameters could be the parameters such as Wake Vortex Turbulence, turbulence energy, and q criterion. Moreover, in the case of using the tendon, the VIV of the mooring could be investigated.
4.5 Breaking/steep wave loads

A important field that S-PIV can play a role is to quantitative estimation of the breaking/steep wave loading on the FOWTs. When breaking wave occurs, a mixture of air and water create a turbulent flow region. This air-sea interface has a complex structure. Regarding the research that is carried out to the date (van der A et al., 2017), the accurate shape and loading of breaking waves is not achieved in literature. Labortory research on breaking wave in deep water is conducted (Ticona Rollano et al., 2019), which was mainly focused on wave breaking rates and wave-following turbulent dissipation. There is also some effort in literature to simulate this phenomena effect on fixed and moored floating with SPH\(^1\) method (Liu et al., 2019). However, as these resercaher reviewed, the magnitude of this phenomena is overestimated by 30% in numerical cases.

The S-PIV could be beneficial here, since it could help to extract instantaneous velocity components and vectors for each sequence of breaking wave. Then, other related parameters of turbulent such as time-dependent turbulent kinetic energy, Reynolds Stress, as well as turbulent production, and dissipation could extracted.

4.6 Wave-current body interaction

Interaction of gravity waves and surface mean flow could have a complex structure, which S-PIV could be utilised to investigate this phenomenon. Current could act as a damping source for long structures (Ye and Ji, 2019). Moreover, the current made frequency shift and shape modification to the wave; hence, the interaction of the incident current and waves to the structure could be the matter of interest in FOWT motion analysis. Research is carried on the wave-current interaction effect on a 5MW FOWT with OC3-Hywind spar floater (Chen and Basu, 2019). In this research, FOWT response under waves with and without current interaction is studied. The result was mainly tower displacement, floater displacements, as well as mooring tensions at Fairlead. In this research, it is showed that the simple method of superposing the wave and current effect causes the overestimation in the response of the FOWT. This difference causes the overestimation of 12% in mooring tension force. The S-PIV could be used for the study of wave kinematic with and without current interaction; the S-PIV velocity and verticity results on this complex turbulent structure could be used for different wave and current propagation angles. Moreover, the floater wave-making in that load cases can be review quantitatively.

\(^1\) Smoothed-particle hydrodynamics
4.7 Viscous load model

The viscous loads are an important load cases in FOWTs analysis, since the viscousity could have different affect on the floater. Among the different phenomena caused by viscousity, the viscous drift forces in extreme sea states (Tan et al., 2021), as well as viscous damping\(^1\) effect (Clement et al., 2021) on floater and mooring line could be mentioned. The point is that the FOWTs models with second-order potential-flow theory usually shows underestimate forces and results, comparing to CFD and lab testing approach (Wang et al., 2021a). This is mainly because of ignoring the separation and viscous drag in potential-flow theory.

As it is proven in literature, the viscosity field for a pseudoplastic flow could captured with S-PIV method (Tiwari et al., 2021). This research is interesting since both momentum conservation, and equation and rheological model are replaced with S-PIV data. Therefore, the viscosity field is examined indirectly. Moreover, it is shown the well known approach in determining the viscosity effects, such as the power law and Carreau-Yasuda model, results in unrealistic increase in viscosity estimation. These kind of research could be restablished for studying of FOWTs and Newtonian fluid. Notably the wake structure and share of pressure, viscosity and kinetic energy in this structure could be visualized and examined.

4.8 Multi-body flow interaction

The S-PIV result could also have a contribution in developing other novel approach in FOWTs analysis, for instance multibody modelling. Many research is carried out in terms of utilising the multibody method for FOWTs analysis, for example (Lemmer et al., 2020), (Ma et al., 2019), and (Al-Solihat and Nahon, 2018); meanwhile some research was mainly focused on coupling this method with numerical methods such as potential theory and CFD (Ma et al., 2019). The S-PIV could have a important, though indirect, contribution in this field. Since the multibody approach is usually coupled with numerical models, such as CFD or BEM method, the S-PIV data could act as an replacement or validation source for hydrodynamic data. A research on uncertainty of CFD method for analysis of FOWTs is conducted in literature (Wang et al., 2021b). In this research, as the researchers examined, the total uncertainty of CFD for estimating the difference-frequency heave force is in the order of 51 percent. Using the underwater S-

\(^1\) Also known as eddy making damping
PIV data, instead of the CFD for coupling with multibody method, could mitigate the relevant errors and uncertainties.

5 Conclusions

There is a need for high-fidelity data to aid the development of the emerging numerical tools and for validation of the new CFD and SPH codes. This paper has presented a review of the use of S-PIV in tank testing campaigns. The S-PIV technique and the technology used have been described, and its application in the fields of marine and offshore engineering has been discussed. It is also discussed that Underwater S-PIV has been used for the hydrodynamical study of other marine and offshore applications, including ship models, tidal stream turbines and propellers. However, the use of S-PIV for hydrodynamic of FOWTs is an emerging field.

It has been discussed that when tank tests only use pitot tube, wave probes and doppler sensors, the hydrodynamical results were generally limited to a certain point that these equipment are installed. Additionally, the use of these instruments results in more manipulation of the fluid flow and measurements error. As an alternative, fluid flow measurement can be conducted with underwater S-PIV. It has been shown that there is a gap between state of the art in tank testing and the demand for new numerical tools. A suitable method to improve the level of experimental campaigns is to combine them with the S-PIV method. The underwater S-PIV approach can easily fill this gap, and with its use, the unsteady structure of turbulent flow around the floater can be measure and understand.

S-PIV is an underutilised technique in FOWT design and has the capacity to provide critical validation data for high fidelity numerical tools. Such data and validated tools will contribute to our understanding of hydrological phenomenon such as those which have been identified by OC5 project as contributing to uncertainty in the design of floating offshore wind turbines. With established best practice guidelines, S-PIV can make a significant contribution to the reduction of uncertainty and ultimate the cost of FOWT.

In the continuation of the current study, the most critical points related to the application of this method in a tank test, moreover its errors and uncertainties, were examined. Additionally, in the current study, the important phenomena related to the hydrodynamic of FOWTs were addressed. As discussed, the underwater S-PIV method is a practical tool to investigate and measure these phenomena. The high-resolution data of the S-PIV later can be used as a validation source for the numerical tools in the field.
Acknowledgements

This research has received funding from the European Union’s Horizon 2020 research and innovation programme under the Marie Skłodowska-Curie grant agreement N° 860879.

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