Characterization of polarimetric and total intensity behaviour of a complete sample of PACO radio sources in the radio bands.

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**ABSTRACT**

We present high sensitivity ($\sigma_P \approx 0.6$ mJy) polarimetric observations in seven bands, from 2.1 to 38 GHz, of a complete sample of 104 compact extragalactic radio sources brighter than 200 mJy at 20 GHz. Polarization measurements in six bands, in the range 5.5 – 38 GHz, for 53 of these objects were reported by Galluzzi et al. (2017). We have added new measurements in the same six bands for another 51 sources and measurements at 2.1 GHz for the full sample of 104 sources. Also, the previous measurements at 18, 24, 33 and 38 GHz were re-calibrated using the updated model for the flux density absolute calibrator, PKS1934-638, not available for the earlier analysis. The observations, carried out with the Australia Telescope Compact Array (ATCA), achieved a 90% detection rate (at 5$\sigma$) in polarization. 89 of our sources have a counterpart in the 72 to 231 MHz GLEAM survey (Hurley-Walker et al. 2017), providing an unparalleled spectral coverage of 2.7 decades of frequency for these sources. While the total intensity data from 5.5 to 38 GHz could be interpreted in terms of single component emission, a joint analysis of more extended total intensity spectra presented here, and of the polarization spectra, reveals that over 90% of our sources show clear indications of at least two emission components. We interpret this as an evidence of recurrent activity. Our high sensitivity polarimetry has allowed a 5$\sigma$ detection of the weak circular polarization for $\sim 38$% of the dataset, and a deeper estimate of 20 GHz polarization source counts than has been possible so far.

**Key words:** galaxies: active – radio continuum: galaxies – polarization.
1 INTRODUCTION

We have undertaken a long-term observational program to characterize the spectra in total intensity and polarization of a complete sample of extragalactic radio sources over an unprecedented frequency range. The sources were drawn from the Planck–ATCA Coeval Observations (PACO) ‘faint sample’ [Bonavera et al. 2011], a complete sample flux-limited at $S_{20\,\text{GHz}} > 200\,\text{mJy}$, extracted from the Australia Telescope Compact Array (ATCA) survey at 20 GHz (AT20G; Murphy et al. 2010), and observed with the ATCA almost simultaneously with Planck observations. The PACO ‘faint sample’ is made up of 159 sources in the South Ecliptic Pole region where Planck’s scan circles intersect, providing maximal sensitivity.

In a previous paper [Galluzzi et al. 2017] we presented high sensitivity (r.m.s. errors $\sigma_p \leq 0.6\,\text{mJy}$; detection rate of about 91%) multi-frequency (six bands, from 5.5 to 38 GHz) polarimetry of a complete sub-sample of 53 compact extragalactic radio sources at ecliptic latitude $<-75^\circ$, observed in September 2014.

In this work we present new ATCA high sensitivity multi-frequency polarimetric observations of a larger complete sample of ‘PACO faint’ sources, now comprising 104 objects. The frequency coverage was also extended adding polarimetric observations at 2.1 GHz. The broader frequency range has allowed a more comprehensive analysis of rotation measures. Moreover, our high sensitivity polarimetry has allowed a 5σ detection of the weak circular polarization for $\sim 38\%$ of data.

The observational determination of total intensity spectra was further extended exploiting the GLEAM (GaLactic and Extra-galactic All-sky Murchison Widefield Array) survey data at 20 frequencies between 72 and 231 MHz [Hurley-Walker et al. 2017], available for 89 ($\sim 86\%$) of our sources.

The paper is organised as follows. In Section 2 we briefly present the observational campaigns. In Section 3 we describe the data reduction. In Section 4 we discuss the data analysis and the spectral behaviours in total intensity and polarization. In Section 5 we present source counts in polarization at $\sim 20\,\text{GHz}$, which is the selection frequency of our sample. Finally, in Section 6 we draw our conclusions.

2 OBSERVATIONS

The new observations were carried out in March and April 2016, using the same array configuration (H214) and spectral setup (three sets of $2 \times 2\,\text{GHz}$ CABB – Compact Array Broadband Backend – bands centred at 5.5–9, 18–24 and 33–38 GHz) as in the previous campaign held in September 2014, whose results are described by Galluzzi et al. (2017). The previous sample of 53 compact extragalactic sources is almost doubled (reaching a total of 104 sources) by adding the ‘PACO faint’ sources at ecliptic latitudes between $-65^\circ$ and $-75^\circ$.

All the 51 additional sources were observed in the six CABB bands. Moreover we re-observed all sources of the September 2014 sample at 5.5 and 9 GHz, while we managed to repeat the observations at 18 – 24 and 33 – 38 GHz only for 20% of them. The whole sample of 104 objects was also observed at 2.1 GHz. We obtained three slots in three contiguous days to have the higher frequencies simultaneously observed. The total observing time was of $\sim 34\,\text{hr}$, including overheads and calibration.

In order to achieve the same sensitivity level of previous observations ($\lesssim 0.6\,\text{mJy}$), we integrated for 1 min at 2.1, 5.5 and 9 GHz, and for 1.5 min at the higher frequencies. The effective sensitivity reached in polarization at 2.1 GHz is a bit worse than requested, $\sim 1\,\text{mJy}$, due to significant radio-frequency interference (RFI). Weather conditions were good during the whole observing campaign. As done for the September 2014 observations, we considered only data from the 5 closest antennas in the H214 array configuration, discarding the baselines to the sixth and farthest antenna, since these are the most noisy. The synthesized beam size ranges from $\sim 90\,\text{arcsec}$ to 5 arcsec in our frequency range.

3 DATA REDUCTION

Data were reduced via the MIRIAD software [Sault et al. 1995]. Each frequency band was treated separately, as indicated in the ATCA User’s Guide. During the data loading, MIRIAD corrects for the time-dependent instrumental xy-phase variation, exploiting the known signal injected from a noise diode, which is mounted in one of the feeds of each antenna.

Our reference for the flux density absolute calibration (at all frequencies) is the source PKS1934-638, a Gigahertz peaked-spectrum (GPS) radio galaxy: it is stable and unpolarized (at least below 30 – 40 GHz) whose last model (see Sault 2003; Partridge et al. 2016) is now loaded into MIRIAD. This introduces a flux density difference with respect to the previous run, so we also re-calibrated the 2014 data. The new flux densities for the 20 GHz data are reported in this paper.

Once the calibration tables were derived, all solutions were ingested in the code for flux density extraction. As we did for the September 2014 observations, to better characterize the source spectra, we decided to split each 2 GHz-wide frequency band in sub-bands, except for the 2.1 GHz one that was kept un-split because of the heavy RFI contamination. Each sub-band was calibrated separately. For total intensity, we split each band into 512 MHz-wide sub-bands. For polarized flux densities we split bands in only 2 sub-bands to limit the $\Delta\nu^{-1/2}$ degradation in sensitivity.

Flux densities were estimated via the MIRIAD task UVFLUX. Our sources are known to exhibit linear polarization (up to $\sim 10\%$; Massardi et al. 2008, 2013), defined by the $Q$ and $U$ Stokes parameters. Observations of the circular polarization of extragalactic radio sources have demonstrated is generally below $0.1 – 0.2\%$, at least one order of magnitude lower than the linear polarization [Rayner, Norris, & Sault 2000]. Hence, the r.m.s. $\sigma_V$ of the retrieved Stokes $V$ parameter is frequently used as a noise estimator.

We achieved a 5σ detection of circular polarization, $V$, in $\sim 38\%$ of the dataset, i.e. $\sim 89\%$ of the objects are detected in Stokes $V$ in at least one frequency.

Further discussion about the circular polarization is in

1 www.narrabri.atnf.csiro.au/observing/users_guide.
2 It is the only known source with all these characteristics in the Southern sky.
sub-sect. 4.5. For only ~ 15% of detections, the circular to linear polarization ratio is ≥ 20%; the mean circular polarization is substantially smaller than our calibration error of the polarized flux density, which is ≃ 10% (Galluzzi et al. 2017). Since the contribution of Stokes V is so small, the polarized emission, P, can be estimated neglecting the V contribution and adopting σv as the r.m.s. noise for the Stokes parameters Q and U:

\[ P = \sqrt{Q^2 + U^2 - \sigma_v^2}. \]  

(1)

The σv term removes the noise bias on P (e.g., Wardle & Kronberg 1974). We find that ignoring the σv term in eq. (1) results in a mean error of 0.01%.

The polarization angle \( \phi \) and fraction \( m \) (usually in terms of a percentage) are:

\[ \phi = \frac{1}{2} \arctan \left( \frac{U}{Q} \right), \]  

(2)

\[ m = 100 \cdot P/I, \]  

(3)

where the Stokes I is the total intensity flux density. The errors in total intensity, linear polarization flux density and position angle were computed as in Galluzzi et al. (2017), i.e. adopting calibration errors of 2.5% for I and of a conservative 10.0% for the polarization fraction, \( P \), for data between 5.5 and 38 GHz. At 2.1 GHz, due to the aforementioned RFI problems, we use a 5% in I and a 12.5% in \( P \) as calibration errors. Under the assumption of equal calibration errors for \( Q \) and \( U \), Galluzzi et al. (2017) reported a ≃ 3σ calibration error in the polarization position angle (3.75° at 2.1 GHz). For circular polarization we again assumed a 10% (12.5% at 2.1 GHz) calibration error (i.e. a factor ≃ \( \sqrt{2} \) larger than the calibration errors associated to \( Q \) and \( U \)). We note however that, due to the weakness of the signal and the corresponding lack of good calibrators, the calibration error for \( V \) is very difficult to estimate.

4 DATA ANALYSIS

We adopt a 5σ level for detections in polarization. The median error is ≃ 0.6 mJy. We reach a detection rate of ≃ 90% for all the sources at all frequencies from 5.5 to 38 GHz. The number of detections is nearly uniform across the observed frequencies (99 sources detected at 5.5 GHz and 94 at 38 GHz). Following Galluzzi et al. (2017) (their Fig. 1) we checked the level of intra-band depolarization in this frequency range, by subdividing each 2 GHz-wide band into 1 GHz-wide sub-bands. No systematic differences were found with respect to the previous assessment. At 2.1 GHz, due to the impact of RFI, we cannot proceed with this check, and the detection rate decreases to ≃ 86%. Three of our 107 observations include the extended source Pictor A. These observations were discarded for the following analysis that therefore deals with 104 compact objects.

4.1 Fit procedures

To fit the spectra we used the same functional forms (a double power-law and a triple power-law) of Galluzzi et al. (2017), and adopted similar criteria about the minimum number of observations to properly constrain the fit parameters. Given the small fraction (less than 10%) of non-detections we do not use upper limits when performing the spectral fitting. About 85% of the spectra could be successfully fitted in this way. In only three cases (AT20GJ041239-833521, AT20GJ054641-641522, AT20GJ062524-602030), we do not have detections in polarization at enough frequencies to get a proper fit.

Similarly to what was found for the earlier sample, most (68%) of our source spectra could be fitted with a double power-law down-turning at high frequencies. An upturning double power-law was required in 15 cases, and a triple power-law in 20 cases. The median values of the reduced \( \chi^2 \) are 1.12 and 1.89 for Stokes I and \( P \), respectively. The spectra for all the sources are presented in Figure 1. The fitting curves and, when available, the previous PACO best epoch (2009–2010) observations in total intensity, and the AT20G best epoch (2004-2008) observations in total intensity and in polarization are also presented. In the lower part of each panel we show the polarization fractions (both linear and circular, when detected), followed by the polarization position angles at the different frequencies.

4.2 Spectral properties of the sample

The spectral index \( \alpha_{\nu_2}^{\nu_1} \) between the frequencies \( \nu_1 \) and \( \nu_2 \) is defined as:

\[ \alpha_{\nu_2}^{\nu_1} = \frac{\log (S(\nu_2)/S(\nu_1))}{\log (\nu_2/\nu_1)}, \]  

(4)

where \( S(\nu_1) \) and \( S(\nu_2) \) are the flux densities associated to the two frequencies. With respect to the previous work (Galluzzi et al. 2017) we simply add the 2.5 GHz to the reference frequencies 5.5, 10, 18, 28 and 38 GHz in order to preserve the equal spacing in logarithmic scale. Then, we proceed as usual for the spectral classification, taking into account \( \alpha_{28}^{38} \) and \( \alpha_{28}^{38} \) and again distinguishing in flat- (F), steep- (S), peaked- (Pe), inverted- (In) and upturning-spectrum (U) object.

We populate the Table 1 with the outcome of the classification performed in total intensity, while

| Pol. Int. ↓ | (In) | (Pe) | (F) | (S) | (U) |
|-------------|-----|------|-----|-----|-----|
| Tot. Int. → |     | 0    | 3   | 0   | 1   | 4   | 0 |
| (In)        | 0   | 24   | 4   | 20  | 0   | 48  |
| (Pe)        | 0   | 5    | 4   | 4   | 0   | 13  |
| (F)         | 0   | 8    | 7   | 0   | 20  |
| (S)         | 0   | 8    | 5   | 3   | 0   | 16  |
| (U)         | 0   | 1    | 1   | 1   | 0   | 3   | 0 |

Table 1. Distribution of sources per spectral type in total intensity and in polarization. The row ‘NA’ refers to the three objects classified in total intensity but missing a spectral fit in polarization.
Figure 1. Spectra in total intensity and polarization, polarization fraction and polarization angle for the 107 objects of the faint PACO sample, observed in the September 2014 and March-April 2016 campaigns. The error bars are not displayed since they are smaller than the symbols. **Total intensity:** red pluses indicate our observations and the solid magenta lines show the fitting curves. The orange crosses show the median PACO flux densities (July 2009-August 2010) while the brown triangles represent the AT20G observations (best epoch in 2004-2008). **Polarization (flux density):** black pluses refer our observations. Upper limits are shown as black filled downwards triangles. The solid blue lines indicate the best fit curves. The AT20G observations (best epoch in 2004-2008) are represented by green diamonds. (Continued...)
Figure 1. (Continued.) Other quantities available only for the September 2014 and March-April 2016 campaigns: linear polarization fractions: purple asterisks with upper limits shown as downwards pointing purple filled triangles; circular polarization fraction: violet circles and downward triangles for upper limits. Polarization angle (PA): black diamonds.
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we report the quartiles of distributions of spectral indices in Table 2. The basic conclusions of our analysis of the earlier, small sample are confirmed: less than 40% of sources have the same spectral behaviour in total intensity and in polarization, and high- and low-frequency spectral indices are essentially uncorrelated, as shown in Fig. 2. The most populated entries of Table 1 are sources peaking both in total intensity and in polarization, and high- and low-frequency spectral indices have the same spectral behaviour in total intensity and in polarization. This change in spectral shape toward a peaked-flat spectrum in total intensity but have a spectral peak in polarization. This is also very similar; the differences with the results by Galluzzi et al. (2017) pointed out that past high frequency flux density measurements may suffer from the low sign of Faraday depolarization which typically lowers the polarization. This change in spectral shape toward a peaked-flat spectrum in total intensity that increases from ∼4% to ∼21%.

To extend the spectral coverage we have exploited the information provided by the GLEAM (Galactic and Extra-galactic All-sky Murchison Widefield Array) survey at 20 frequencies between 72 and 231 MHz (Hurley-Walker et al. 2017). The spatial resolution is ∼2 arcmin at 200 MHz, similar to the ∼9 arcsec resolution of our 2.1 GHz observations. We have 89 matching sources (∼86% of our sample) in the GLEAM survey. For these sources we have the unparalleled coverage of 2.7 decades in frequency. Since the GLEAM survey covers all the sky south of +30° in declination with a mean sensitivity of ∼10 mJy, and our sample is located between −86° and −42°, we can associate an upper limit of 50 mJy (at 5σ) to those sources without a GLEAM counterpart.

The fitting curves (triple power-laws), although not always successful, generally show a good consistency between the ATCA and GLEAM measurements (cf. Fig. 1). But while in the range 5.5 GHz − 38 GHz the spectra are consistent with a single emitting region (Galluzzi et al. 2017), the GLEAM flux densities are clearly above the extrapolations from higher frequencies in ∼40% of the cases, strongly suggesting the presence of at least another, generally steeper, component. The joint analysis with polarization data suggests even more complex structures (cf. Farnes et al. 2014; see sub-section 4.3).

Table 2. First, second (median), and third quartiles of spectral indices in total intensity and in polarization for different frequency ranges. We give values for the full sample and for the three main spectral classes, as classified in total intensity.

| Tot. Int. | 2.5 − 5.5 | 5.5 − 10 | 10 − 18 GHz |
|-----------|-----------|----------|------------|
| Quart. | Q1 | Q2 | Q3 | Q1 | Q2 | Q3 | Q1 | Q2 | Q3 |
| All | -0.29 | -0.02 | 0.31 | -0.35 | -0.11 | 0.09 | -0.46 | -0.24 | -0.08 |
| Steep | -0.64 | -0.33 | -0.13 | -0.67 | -0.37 | -0.22 | -0.80 | -0.46 | -0.30 |
| Peaked | 0.10 | 0.32 | 0.54 | -0.04 | 0.06 | 0.27 | -0.30 | -0.14 | 0.01 |
| Flat | -0.16 | -0.01 | 0.27 | -0.25 | -0.12 | 0.06 | -0.26 | -0.14 | -0.05 |

| Pol. Int. | 2.5 − 5.5 | 5.5 − 10 | 10 − 18 GHz |
|-----------|-----------|----------|------------|
| Quart. | Q1 | Q2 | Q3 | Q1 | Q2 | Q3 | Q1 | Q2 | Q3 |
| All | -0.28 | 0.15 | 0.85 | -0.43 | -0.06 | 0.38 | -0.61 | -0.15 | 0.34 |
| Steep | -0.46 | 0.33 | 0.61 | -0.59 | -0.06 | 0.33 | -0.74 | -0.24 | 0.29 |
| Peaked | -0.06 | 0.49 | 1.04 | -0.19 | -0.01 | 0.71 | -0.35 | -0.06 | 0.36 |
| Flat | -0.57 | -0.21 | -0.06 | -0.54 | -0.29 | -0.06 | -0.59 | -0.33 | 0.54 |

| Pol. Int. | 18 − 28 | 28 − 38 GHz |
|-----------|---------|------------|
| Quart. | Q1 | Q2 | Q3 | Q1 | Q2 | Q3 |
| All | -0.98 | -0.53 | 0.02 | -1.44 | -0.80 | -0.03 |
| Steep | -1.00 | -0.76 | -0.10 | -1.47 | -0.92 | -0.37 |
| Peaked | -0.80 | -0.32 | 0.31 | -1.21 | -0.73 | -0.23 |
| Flat | -1.01 | -0.54 | 0.14 | -1.61 | -0.68 | 0.04 |
Figure 2. Radio colour-colour diagrams for (from left to right) total intensity and polarized flux density. Symbols identify the spectral type in total intensity: pluses for flat-spectrum, asterisks for steep-spectrum, diamonds for peaked-spectrum. Colours refer to the spectral shape between 5.5 and 18 GHz: red for steep-spectrum, blue for flat-spectrum, and green for peaked-spectrum sources.

Figure 3. Spectra in total intensity and polarization taking into account GLEAM observations between 72 and 231 MHz (orange pluses). Our observations in total intensity are the red pluses, while black pluses and downward triangles are for polarization. The fits in total intensity and polarization are given as red and black solid curves, respectively. We report the SUMSS (Sydney University Molonglo Sky Survey, Mauch et al. (2003)) flux density at 843 MHz just for comparison, but we do not use it in the fit procedures. For each object, after its name, spectral indices (computed in total intensity) $\alpha_{0.5}$, $\alpha_{2.5}$ and $\alpha_{28}$ are provided. At the end of the title of each plot there is the spectral classification in terms of estimated synchrotron components (see 4.3).
4.3 Linear polarization fraction

Galluzzi et al. (2017) did not find any systematic variation of the mean polarization fraction with either flux density or frequency, down to \( \sim 5 \) GHz, in agreement with the results by Massardi et al. (2013). A similar conclusion was reached by Battye et al. (2011), who however had measurements only down to 8.4 GHz. On the other hand, claims of a systematic decrease of the polarization fraction with decreasing frequency were made by Agudo et al. (2010, 2014) and Sajina et al. (2011), suggesting that Faraday depolarization may work up to \( \sim 10 \) GHz or that the magnetic field is more ordered at high frequencies (Tucci et al. 2004). However the conclusions by Agudo et al. (2010, 2014) and Sajina et al. (2011) may be biased towards greater polarization fractions by not having taken into account non-detections (Tucci & Toffolatti 2012).

Our new observations allowed us to extend the spectra in polarized intensity down to 2 GHz and to have a factor of 2 larger sample. As for Galluzzi et al. (2017), our high detection rate (over 90%) safeguards against any selection bias. Although the polarization fraction declines for several sources drops at lowest frequency (cf. Fig. 1), there is no statistical evidence of a decrease of the mean value for the whole sample or for its sub-samples. However, as discussed below, such apparent uniformity may hide a more complex situation. The steep-spectrum objects (36) indeed show a slight trend, but comparing to the distributions of polarization fraction at 2.1 and 38 GHz, the rejection of the null hypothesis reaches the \( \sim 2 \sigma \) level. The sample of flat-spectrum objects (22 objects in total) seems to reveal an opposite trend, but also in this case the significance is less than 3\( \sigma \).

The spectra of the polarization fraction are less smooth than the total intensity spectra. Only about 15% of the sources have an approximately constant polarization fraction over the full frequency range. Five sources with smooth total intensity spectra above 2 GHz have double peaked fractional polarization, suggesting at least two emission components, seeing different screens. The polarization fraction of \( \sim 15\% \) of the sources has an upturn at 2 GHz, where the emission components seen in the GLEAM data may yield a substantial contribution. The polarized flux from these components can drown out the decrease of the polarization fraction of the higher frequency component, due to Faraday depolarization. The most straightforward interpretation of these results is that the extension (and, correspondingly, the age) of emission components increases with decreasing frequency.

On the whole, a joint inspection of total intensity (including GLEAM measurements between 72 MHz and 231 MHz) and polarization spectra indicates the presence of at least 2 (sometimes 3) emission components for about 93\% of the sources. This is expected for GPS/CSS sources due to their double lobe structure (Lingay & de Kooi 2003, Gallimore et al. 2015). For about half of these, the clearest indication comes from polarization data. Hence, we reclassify our sample by distinguishing cases in which there is no sign of an additional synchrotron component (we label it ‘1C’) from situations in which there are hints of 2 – 3 synchrotron components (‘2-3C’) or more complicated cases which seems to reveal more than 3 components in the spectrum. The latter are quite flat sources in total intensity from 70 MHz up to \( \sim 30 \) GHz, where a steepening typically occurs. Among these 17 objects (\( \sim 16\% \)) 10 are classified in the flat (F) spectral category, i.e. objects with a flat spectrum in total intensity between 2.1 and 38 GHz.

According to Fig. 3 we do not have evidences of trends of the linear polarization fraction with the frequency for the full sample and for ‘1C’ sources. ‘2-3C’ sources have a minimum of the polarization fraction at \( \sim 9 \) GHz, consistent with different emission components at lower and higher frequencies. For the >3C objects, whose spectra show indications of several overlapping synchrotron components, there is a hint of a decrease with increasing frequency (rather than of the increase expected by some authors, see e.g. Tucci & Toffolatti 2012) of the polarization fraction: the mean values decline from \( \sim 2.1 – 2.4\% \) at \( \leq 5.5 \) GHz to 1.2\% at 38 GHz. We anticipate here that in sub-section 4.4, we find these sources to have very large rotation measures (RMs) at mm wavelengths. This could indicate that their high frequency components are characterised by a really dense and/or a magnetised medium that rotates the polarisation angle strongly (cf. Pasetto et al. 2016).

4.4 Polarization angle: cm- and mm-wavelength regime behaviour

The polarization angle was calibrated setting the parameter ‘xcorr’ in the MIRIAD task ATLOD which applies phase corrections provided by a noise diode mounted on one antenna feed. Partridge et al. (2016) found that the polarization angles measured by ATCA in this way agree with those measured by Planck based on the CMB dipole measurements to within \( \pm 2^\circ \).

Galluzzi et al. (2017) found evidence of non-zero Faraday rotation for only 2 objects (over a total of 53), since for the overwhelming majority of the sources the dependence of the rotation measure (RM) with \( \lambda^2 \) has a complex behaviour. Only 9 objects of our larger sample can be described by a linear \( \text{RM} - \lambda^2 \) relation over the our full frequency range (2.1–38 GHz). For these sources RM estimates are between \(-72\) and \(57\) rad/m\(^2\), with 4 cases compatible with a low (\( \sim \pm 10\) rad/m\(^2\)) or a null rotation.

Exploiting our larger frequency range, we can identify two regimes for the \( \text{RM} vs \lambda^2 \) relation, one at cm-wavelengths and the other at mm-wavelengths. We have investigated this more complex scenario by fitting the polarization angle as a function of the \( \lambda^2 \) separately for the two regimes (from 2.1 to 9 GHz and from 18 to 38 GHz). We required at least three measured polarization angles in each regime to perform the fit via the IDL ‘linfit’ procedure. A fit was regarded as acceptable when the reduced \( \chi^2 \) was less than 2 (probability > 0.1). We obtained \(~ 40\%\) and \(~ 57\%\) successful fits for the low and high frequency regimes, respectively. The corresponding median values of the reduced \( \chi^2 \) are 0.37 and 0.69, respectively.

The medians and quartiles at cm- and mm-wavelengths are reported in Table 4 for both all objects for which acceptable fits were obtained and for the ‘1C’, ‘2-3C’ and ‘>3C’ types, defined in sub-section 3.3. We warn the reader that the error associated to the estimated RMs can be large especially at the higher frequencies because of its dependence on \(1/\lambda^2 \). Typical uncertainties are of about 9\% and 32\% at low
The circularly polarized emission is weak, typically $\lesssim 0.1\%$ (Rayner, Norris, & Sault 2000), but potentially very interesting because its measurements may permit to gain information on various properties of jets, such as magnetic field strength and topology, the net magnetic flux carried by jets (and hence generated in the central engine), the energy spectrum of radiating particles, and the jet composition, i.e. whether jets are mainly composed of electron-positron pairs or electron-proton plasma (Ruszkowski & Begelman 2002).

The most obvious candidate for explaining circular polarization of compact radio sources is intrinsic emission, but the expected level under realistic conditions appears to be too low to explain the observed polarization (Warde & Homan 2003, Pacholczyk 1973) pointed out that magnetic fields computed from the circular polarization, assuming that it is intrinsic, are usually so high as to cause a turnover in the intensity spectrum through synchrotron self-absorption at a considerably higher frequency than is actually observed. The most promising mechanism is Faraday conversion, a birefringence effect that converts linear to circular polarization of compact radio sources is intrinsic emission, but the expected level under realistic conditions appears to be too low to explain the observed polarization (Warde & Homan 2003, Pacholczyk 1973) pointed out that magnetic fields computed from the circular polarization, assuming that it is intrinsic, are usually so high as to cause a turnover in the intensity spectrum through synchrotron self-absorption at a considerably higher frequency than is actually observed. The most promising mechanism is Faraday conversion, a birefringence effect that converts linear to circular polarization (Warde & Homan 2003, Pacholczyk 1973) pointed out that magnetic fields computed from the circular polarization, assuming that it is intrinsic, are usually so high as to cause a turnover in the intensity spectrum through synchrotron self-absorption at a considerably higher frequency than is actually observed. The most promising mechanism is Faraday conversion, a birefringence effect that converts linear to circular polarization (Warde & Homan 2003, Pacholczyk 1973) pointed out that magnetic fields computed from the circular polarization, assuming that it is intrinsic, are usually so high as to cause a turnover in the intensity spectrum through synchrotron self-absorption at a considerably higher frequency than is actually observed. The most promising mechanism is Faraday conversion, a birefringence effect that converts linear to circular polarization (Warde & Homan 2003).
Characterization of a complete sample in the radio bands

Table 4. Median plus I and III quartile values of cm-wavelengths (upper table) and mm-wavelengths (lower table) RMs. In each table the upper set of values refers to the observed RMs while the lower set refers to the RMs at the source for the subset of sources for which redshift measurements are available. In parenthesis are the numbers of sources in each group. Whenever the number of objects is < 10 we provide only the median value. RMs are in rad/m^2.

| All sample (42) | 1C (3) | 2-3C (31) | >3C (8) |
|-----------------|--------|-----------|---------|
| I med III       | I med III | I med III | I med III |
| 18 37 58        | - 60 - | 15 34 53  | - 37 -  |
| All sample (23) | 1C (2) | 2-3C (18) | >3C (3) |
| I med III       | I med III | I med III | I med III |
| 40 94 244       | - 335 - | 46 84 220 | - 122 - |

| All sample (59) | 1C (4) | 2-3C (50) | >3C (5) |
|-----------------|--------|-----------|---------|
| I med III       | I med III | I med III | I med III |
| 225 635 1397    | - 342 - | 283 637 1397 | - 1141 - |
| All sample (27) | 1C (2) | 2-3C (22) | >3C (3) |
| I med III       | I med III | I med III | I med III |
| 679 2300 5252   | - 742 - | 716 2351 5191 | - 4022 - |

Figure 4. Median polarization fraction behaviour with frequency (at 2.1, 5.5, 9, 18, 24, 33 and 38 GHz) for all the sources (black), for steep sources (red), for peaked (green) and flat ones (blue). The errors on median values are given by 1.253 × rms/√N, where rms is the standard deviation around the mean and N is the number of the data (at a given frequency) for a given class of objects (cf. Arkin & Colton 1970).

Figure 5. Median polarization fraction at the observation frequencies (2.1, 5.5, 9, 18, 24, 33 and 38 GHz) for all the sources (black), for ‘1C’ sources (red), for ‘2-3C’ sources (green) and for sources with more than 3 components (blue, labelled ‘>3C’). The errors on median values are given by 1.254 × rms/√N, where rms is the standard deviation around the mean and N is the number of detected sources (cf. Arkin & Colton 1970).
larger median values may be due to the fact that, because of the higher selection frequency, the overwhelming majority of objects in our sample are blazars. Rayner, Norris, & Sault (2000) have found that these objects have larger circular polarization fractions than radio galaxies that comprise a significant fraction (≃ 25%) of their sample.

5 SOURCE COUNTS IN POLARIZATION

Figure 7 shows the source counts in polarization at 20 GHz obtained through the convolution of the total intensity differential source counts reported by the model De Zotti et al. (2005) with our distribution of polarization fractions at 18 GHz. In the Table 5 and in the Figure 6 we report the observed distribution (black circles): in each bin uncertainties are derived assuming a Poisson statistics, following the indications of Gehrels (1986). The solid line is the fit assuming a log-normal distribution

\[ f(\Pi) = \text{const} \cdot \frac{1}{\sqrt{2\pi} \sigma \Pi} \exp \left( -\frac{1}{2} \left( \frac{\ln(\Pi/\Pi_\text{m})}{\sigma} \right)^2 \right), \tag{6} \]

where const = 0.96, \( \sigma = 0.76 \) and \( \Pi_\text{m} = 2.00 \), i.e. the median value of the distribution. The reduced \( \chi^2 \) value is 0.21. In the Table 5 and in the figure 7 (black circles) we plot the differential source counts in polarization, following the recipe reported by Tucci & Toffolatti (2012): since there is no evidence of a correlation between the total intensity flux density and the polarization fraction, the number counts \( n(P) = \frac{dN}{dP} \) can be determined by

\[ n(P) = \int_{S_0 = P}^{\infty} \mathcal{P} \left( m = \frac{P}{S} \right) n(S) \frac{dS}{S}, \tag{7} \]

where \( n(S) \) is the assumed source counts in total intensity, \( \mathcal{P} \) is the probability density distribution for the polarization fraction \( m \), i.e. \( \Pi/100 \). Note that in each bin in \( P \) the integration over \( S \) is truncated at \( S_0 = P \), which corresponds to the maximum degree of the polarization fraction (i.e. \( m = 1.0 \)). We compare our results with source counts provided by Massardi et al. (2013, blue diamonds) via a MCMC simulation of the whole AT20G catalogue (Massardi et al. 2011a), as well as with the Tucci & Toffolatti model (2012, red and blue lines, which refer to the lower and upper level respectively). Since our sample is mainly composed by blazars (BL Lacs and FSRQs), which typically are labelled as ‘flat’ and represent the dominant population at 20 GHz (dashed lines), we expect and find a good agreement with the limits on the total source counts provided by the model. Hence, given the assumptions of Tucci & Toffolatti (2012) on the median polarization fraction of steep-spectrum radio sources (presented in their Table 4), that are higher than our current findings (see our Figure 5, for a comparison), their overestimation of source number counts in polarization below 10 mJy can be (at least partially) explained. Note that eq. (7) assumes independence of the polarization fraction from the total flux density. However this assumption can be broken as another population, namely steep-spectrum sources, with different polarization properties, becomes increasingly important with decreasing flux density.

|\( \Pi \) (per cent)| Probability| lower uncert. | upper uncert. |
|---|---|---|---|
|0.600| 0.2404| 0.0453| 0.0453|
|1.800| 0.2644| 0.0446| 0.0446|
|3.000| 0.1843| 0.0381| 0.0470|
|4.200| 0.0721| 0.0222| 0.0317|
|5.400| 0.0321| 0.0153| 0.0253|
|6.600| 0.0160| 0.0104| 0.0211|
|7.800| 0.0160| 0.0104| 0.0211|
|9.000| <0.01843| | |
|10.200| <0.00801| | |
|11.400| 0.0080| 0.0066| 0.0184|

Figure 6. Distribution of the polarization fraction at 18 GHz. Errors and upper limits correspond to a 1σ level. The black circles refer to the sample studied in this paper, the red pluses to the full AT20G bright sample studied in Massardi et al. 2013. The corresponding fit by a log-normal distribution for each dataset is reported with a solid lines of the same color.

6 CONCLUSIONS

We have presented and discussed high sensitivity polarimetric observations in 7 bands, centered at 2.1, 5.5, 9, 18, 24, 33 and 38 GHz, of a complete sample of 104 extragalactic sources with \( S_{20\text{GHz}} \geq 200 \text{mJy} \) in the AT20G catalogue. The r.m.s error in the polarized flux density is 0.6 mJy at \( \nu \geq 5.5 \text{GHz} \) and 1 mJy at 2.1 GHz, due to the heavy RFI contamination.

Polarization measurements in the range 5.5 – 38 GHz for 53 objects of the sample were reported by Galluzzi et al. (2017). The measurements for the other 51 sources are new, as are the 2.1 GHz measurements for the full sample of 104 sources. The 53 sources were re-observed at 5.5 and 9 GHz, while we managed to repeat the observations at 18, 24, 33 and 38 GHz only for 20% of them. The previous measurements at 33 and 38 GHz were re-calibrated using the updated model for the flux density absolute calibrator, PKS1934-638, that was not available for the earlier analysis.

The observational determination of the continuum spectra has been extended by exploiting the GLEAM survey data at 20 frequencies between 72 and 231 MHz (Hurley-Walker et
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Table 6. Euclidean normalized differential source counts at 20 GHz in polarization obtained in this paper via the convolution of the distribution of the polarization fraction at 18 GHz with the De Zotti model (2005).

| \( \log[P(Jy)] \) | \( S^{-3/2}n(S) \) (Jy\(^{-3/2}\) sr\(^{-1}\) ) | lower uncert. | upper uncert. |
|----------------|------------------|----------------|----------------|
| -2.897 | 0.0667 | 0.0007 | 0.0007 |
| -2.692 | 0.0760 | 0.0011 | 0.0011 |
| -2.486 | 0.0869 | 0.0017 | 0.0017 |
| -2.281 | 0.1011 | 0.0025 | 0.0025 |
| -2.075 | 0.1198 | 0.0039 | 0.0039 |
| -1.870 | 0.1426 | 0.0061 | 0.0061 |
| -1.664 | 0.1662 | 0.0094 | 0.0094 |
| -1.459 | 0.1856 | 0.0142 | 0.0142 |
| -1.253 | 0.1978 | 0.0209 | 0.0209 |
| -1.048 | 0.1987 | 0.0299 | 0.0299 |
| -0.842 | 0.1886 | 0.0417 | 0.0519 |
| -0.637 | 0.1734 | 0.0549 | 0.0766 |
| -0.431 | 0.1580 | 0.0726 | 0.1199 |
| -0.226 | 0.1447 | 0.0996 | 0.2034 |
| -0.020 | 0.1337 | 0.1297 | 0.3606 |
| 0.185 | <0.011886  | |
| 0.391 | <0.64841 | |
| 0.596 | <1.31855 | |

Figure 7. Differential source counts at 20 GHz in polarization obtained in this paper plotted with black circles (black downward triangles are for upper limits). Also shown, for comparison, are the estimates by Massardi et al. (2013) using the polarimetric data from their own survey, somewhat shallower than the present one (\( S_{20 \text{ GHz}} > 500 \text{ mJy} \)) combined with the full AT20G catalogue (blue diamonds and blue downward triangles for upper limits). The curves show the predictions of the Tucci & Toffolatti (2012) model: blue curves for the ‘conservative’ case and red curves for the ‘optimistic’ case. The solid lines represent the total number counts; the dotted lines are for steep-spectrum sources (classified at low frequencies); the dashed lines are for flat objects (flatspectrum radio quasars, i.e. FSRQs and BL Lacs).

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