Nonthermal Emission from Fall-back Clouds in the Broad-line Region of Active Galactic Nuclei

Ana Laura Müller1, Mohammad-Hassan Naddaf2,3, Michal Zajáček2,4, Bozena Czerny2, Anabella Araudo1,5,6, and Vladimir Karas6

1 ELI Beamlines, Institute of Physics, Czech Academy of Sciences, CZ-25241 Dolní Břežany, Czech Republic; analaura.muller@eli-beams.eu
2 Center for Theoretical Physics, Polish Academy of Sciences, Al. Lotników 32/46, 02-668 Warsaw, Poland
3 Nicolaus Copernicus Astronomical Center, Polish Academy of Sciences, Bartycka 18, 00-716 Warsaw, Poland
4 Department of Theoretical Physics and Astrophysics, Faculty of Science, Masaryk University, Kotlářská 2, CZ-611 37 Brno, Czech Republic
5 Laboratoire Univers et Particules de Montpellier (LUPM) Université Montpellier, CNRS/IN2P3, CC72, place Eugène Bataillon, F-34095, Montpellier Cedex 5, France
6 Astronomical Institute, Czech Academy of Sciences, Boční II 1401, CZ-141 00 Prague, Czech Republic

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Abstract

The spectra of active galactic nuclei exhibit broad-emission lines that presumably originate in the broad-line region (BLR) with gaseous-dusty clouds in a predominantly Keplerian motion around the central black hole. Signatures of both inflow and outflow motion are frequently seen. The dynamical character of BLR is consistent with the scenario that has been branded as the failed radiatively accelerated dusty outflow. In this scheme, frequent high-velocity impacts of BLR clouds falling back onto the underlying accretion disk are predicted. The impact velocities depend mainly on the black hole mass, accretion rate, and metallicity, and they range from a few km s\(^{-1}\) up to thousands of km s\(^{-1}\). Formation of strong shocks due to the collisions can give rise to the production of relativistic particles and associated radiation signatures. In this work, the nonthermal radiation generated in this process is investigated, and the spectral energy distributions for different parameter sets are presented. We find that the nonthermal processes caused by the impacts of clouds can lead to emission in the X-ray and the gamma-ray bands, playing the cloud density and metallicity key roles.

Unified Astronomy Thesaurus concepts: Nonthermal radiation sources (1119); Shocks (2086); Active galactic nuclei (16); Galaxy accretion (575); Emission line galaxies (459)

1. Introduction

The spectra of active galactic nuclei (AGNs) display distinctive features across a broad range of frequencies, suggesting that these regions contain many different components (see e.g., Antonucci 1993; Urry & Padovani 1995; Karas et al. 2021). Nevertheless, the inability to resolve such compact and bright regions using the current instruments challenges unveiling the AGN structure in detail. In particular, the characteristic broad-emission lines of type-I AGNs (Seyfert 1943; Wolter 1959; Schmidt 1963) are assumed to be produced very close to the central supermassive black hole (BH), in the so-called broad-line region (BLR). According to the observational data, BLRs are made up of clouds moving primarily in Keplerian orbits (see e.g., Peterson et al. 1998; Shapovalova et al. 2010; Grier et al. 2013). Additionally, the measured lines indicate the presence of inflowing and outflowing matter (see e.g., Brotherton et al. 1994; Done & Kroll 1996; Doroshenko et al. 2012), confined in a flattened region (Gravity Collaboration et al. 2018). Although the origin of these line-emitting clouds remains unknown, this particular geometry hints that they are likely related to the accretion disk, at least pertaining to the clouds of the low-ionization line BLR part.

Over the years, several models were developed to explain the formation, dynamics, and emission lines of BLRs (Osterbrock 1978; Blandford & Payne 1982; Begelman & McKee 1983; Murray et al. 1995; Done & Krolik 1996; Hu et al. 2008; Collin & Zahn 1999; Czerny & Hryniewicz 2011; Wang et al. 2011; Baskin & Laor 2018). These clouds have also been considered to participate in processes that can produce and absorb high-energy photons (Dar & Laor 1997; Araudo et al. 2010; del Palacio et al. 2019; Tavecchio & Ghisellini 2012; Böttcher & Els 2016; Britzen et al. 2021). However, in most of these studies, the geometry of the BLR is assumed to be spherical and the radial distribution of clouds uniform.

In this work, we aim to study the nonthermal features connected with a realistic flattened BLR description. Particularly, we discuss the BLR properties as expected from the failed radiatively accelerated dusty outflow (FRADO) model (Czerny & Hryniewicz 2011; Czerny et al. 2015, 2016, 2017; Naddaf et al. 2020, 2021; Naddaf & Czerny 2021). In this model, the formation of BLR clouds is governed by the radiation pressure of the accretion disk acting on dust grains, analogously as it is inferred in dusty stellar winds, e.g., in asymptotic giant branch (AGB) stars (see e.g., Sedlmayr & Dominik 1995). At distances where the temperature of the accretion disk drops below the dust sublimation temperature, the local radiation pressure is large enough to expel material from the disk. Once the cloud elevates above the disk, the photons coming from the hot inner part of the AGN illuminate the plasma, increasing the temperature, and producing the sublimation of the dust. Without dust, the cloud is not sensitive to the radiation pressure anymore and starts to move by following a ballistic motion, first upwards and finally falling...
back onto the accretion disk. The production of shocks and nonthermal emission in such cloud impacts was recently proposed and studied by Müller & Romero (2020). In their work, the authors found that the emitted radiation can significantly contribute to the X-ray and gamma-ray emission of AGNs.

In this paper, we investigate the nonthermal characteristics within the BLR in the scenario investigated by Müller & Romero (2020) (see Figure 1), when the cloud dynamics and impacts are described by the 2.5D FRADO model (Naddaf et al. 2021). In Section 2, we refer to the FRADO model and display the parameters explored in our analysis. We examine the feasibility of accelerating particles due to disk-cloud collisions in Section 2.4. Our results are shown in Section 3. Finally, Section 4 presents a summary and our conclusions. The implications of the assumptions we made, in particular the cloud stability, are discussed in the Appendix.

2. The BLR Dynamics in the FRADO Model

The FRADO model describes the dynamics of the BLR clouds in a non-hydrodynamic, simple way. A fully analytical form of this approach was first proposed by Czerny & Hryniewicz (2011), and later developed in more detail (Czerny et al. 2015, 2017). The description of the full 3D cloud motion requires semi-numerical calculations that were recently presented in Naddaf et al. (2020, 2021) and Naddaf & Czerny (2021). The clouds are considered to be launched by the dust-driven outflow. Nevertheless, the rise of their height above the disk increases the exposure to the radiation from the disk’s central parts, causing the dust sublimation. This effect is taken into account in the model, which reproduces reliably the radius-luminosity relation in the low-ionization part of the BLR, at the basis of the assumed value of the dust sublimation temperature.

We calculate the dynamical properties of the BLR as described in Naddaf et al. (2021). The accretion disk is modeled using a Shakura–Sunyaev disk model with a proper account of the disk vertical structure and internal opacity (Różańska et al. 1999; Czerny et al. 2016), which is important for an accurate determination of the disk thickness as a function of radius. The clouds are ejected from the disk surface and move under the influence of the radiation pressure acting on the dust inside the cloud. The radiation pressure comes mainly from the patch of the disk underlying the cloud, i.e., it is a function of the cloud location and increases with the cloud height. This approach takes into account the shielding of the central source by other clouds and by the inner line-driven wind.

The innermost radius of the BLR (BLRin) is found by requiring the radiation pressure to be strong enough to lift the clouds, but the temperature must still be below the sublimation threshold. For given values of BH mass (MBH) and accretion rate (Ṁ), this BLRin depends on the assumed value of the dust sublimation temperature. The computational grid covers the disk densely, with a constant step, linear in radius. The outer edge of the BLR (BLRout) is set by the location of the dusty/molecular torus. When the cloud is launched, we follow its trajectory. At each trajectory point, the dust temperature in the cloud is obtained from the dust thermal equilibrium. Once this temperature exceeds the sublimation temperature, the radiation pressure is turned off, and the cloud follows a ballistic trajectory. It is important to note that the gas temperature in the cloud (~10^4 K) is generally much higher than the dust temperature, i.e., there is no thermal equilibrium between the dust and the gas due to the large difference in their heating and cooling mechanisms. However, we assume an efficient dust and gas Coulomb coupling; thus, the gas hitchhikes with dust.

2.1. Model Parameters

We consider two exemplary values of the BH mass: \( M_{\text{BH}} = 10^6 \) and \( 10^8 M_{\odot} \), appropriately covering the most common parameter range observed in the AGNs. As the FRADO model is sensitive to the Eddington ratio \( \dot{m} = \dot{M}/\dot{M}_{\text{Edd}} \), we study three different values: 0.01, 0.1, and 1.0, as in Naddaf et al. (2021) and Naddaf & Czerny (2021). Because the observational evidence has pointed out that the metallicity Z in the AGNs is likely super-solar (see e.g., Hamann & Ferland 1992; Artyomowicz et al. 1993; Ferland et al. 1996; Hamann 1997; Dietrich et al. 2003; Xu et al. 2018; Sniegowska et al. 2020), we adopt two extreme values: \( Z = Z_{\odot} \) and \( SZ_{\odot} \), where \( Z_{\odot} \) is the solar metallicity. Specifically, \( Z > Z_{\odot} \) enhances the radiation pressure acting on the dust, and leads to a more vigorous outflow.

In all the models, we use the wavelength-dependent dust opacity from Röllig et al. (2013), adopting a mixture of graphite and silicate grains with the standard range of grain sizes (see Naddaf et al. 2021 for details). We assume that the dust sublimation temperature is 1500 K. Cloud launching requires some shielding, and for all the models we fixed the shielding parameter (\( \alpha \)) describing the fraction of the disk surface seen by the cloud at each point of its trajectory at \( \alpha = 3 \) (see Naddaf et al. 2021 for more details).

For the purpose of this work, we adopt cloud number densities \( n_c = 10^{11}, 10^{12} \text{ cm}^{-3} \) and hydrogen column densities \( N_H = 10^{23}, 10^{24} \text{ cm}^{-2} \), respectively, from which we estimate the characteristic cloud length-scale, \( R_c \sim N_H/n_c = 10^{-2} \text{ cm} \). The characteristic cloud mass, then, is \( M_c = (4/3)\pi R_c^3 n_c m_p \sim 2 \times 10^{-9} M_\odot \sim 4 M_{\text{Ceres}} \), where \( M_{\text{Ceres}} \) is the Ceres mass. A summary of the important initial parameters of the model is provided in Tables 1 and 2. In the latter, \( r_{\text{g}} \) and \( M_{\text{E}} \) are the gravitational radius and the Eddington accretion rate for a BH of \( 10^6 M_{\odot} \), respectively.
2.2. Cloud Fall-back onto the Accretion Disk

In the low Eddington accretion regime, all clouds form a failed wind, and their departure from the launching radius becomes relatively small. Consequently, the motion of such clouds under the radiation pressure acting on dust is well approximated by the plane-parallel approach, as argued by Czerny et al. (2015). Because the clouds cover the disk surface uniformly, albeit each of them at a different phase of motion, their impact rate onto the disk can be determined by the duration of the orbital motion. However, the plane-parallel approach cannot be applied for cases with high Eddington rates. This is because a stream of high-velocity clouds forms close to the inner BLR radius for such cases, and those clouds either hit the torus or all fall down onto the disk very far away from their starting point.

Although the model determines precisely the velocity field of the clouds, it cannot predict directly the local stream of the launched material. To overcome this difficulty, we divide the clouds into two populations: local clouds that form a local failed wind, mostly observed in the outer disk part, and nonlocal clouds from a stream that can be described using a standard approach like in stellar or disk winds. We define these two categories based on the relative difference between the starting radius of the clouds, \( r_{\text{launch}} \), and their landing radius, \( r_{\text{impact}} \). Nonlocal clouds should satisfy

\[
\frac{|r_{\text{impact}} - r_{\text{launch}}|}{r_{\text{launch}}} > 0.1. \tag{1}
\]

This criterion allows us to distinguish both populations and calculate their impact rate onto the accretion disk. The existence of one or two groups of clouds depends on the parameters adopted for a specific model. For instance, in cases with a low Eddington rate and/or low metallicity, only the local clouds are present.

2.3. Impact Rate

In the case of the local clouds, we assume that they cover uniformly the disk surface while performing their up-and-down motion (Czerny et al. 2015). Numerically, we consider trajectories with starting points \( r_{\text{launch}} \) distributed equidistantly along the disk surface. For each trajectory, we compute the time \( t_{\text{flight}} \) needed to complete the path between the launching and landing points. We thus calculate the impact rate \( \dot{N} \) per unit surface of local clouds at the impact distance \( r_{\text{impact}} \) as

\[
\dot{N}(r_{\text{impact}}) = \frac{1}{t_{\text{flight}}} R_c^2, \tag{2}
\]

where \( R_c \) is the radius of the cloud.

For the nonlocal clouds, the assumption of the uniform coverage is not appropriate because their launching mechanism is similar to that of an escaping wind. Therefore, we apply the approach developed by Murray et al. (1995) for line-driven winds. We assume that the total local radiation flux \( F(r) \) at the launching radius \( r_{\text{launch}} \) is used by the cloud to get an initial velocity equal to the local sound speed \( C_s \) in the disk atmosphere. Under this condition, the impact rate of nonlocal clouds can be written as

\[
\dot{N}(r_{\text{impact}}) = \frac{F(r_{\text{launch}})}{C_s m_p n_c R_c^3} f(r_{\text{launch}}, r_{\text{impact}}), \tag{3}
\]

where \( f(r_{\text{launch}}, r_{\text{impact}}) \) is defined as the ratio of the surfaces of the launching ring to the corresponding impact ring, which can be very different in this case. To adopt \( C_s \) instead of escaping velocity of the wind may seem to be a serious limitation, but the driving flux increases as the cloud rises higher above the disk and becomes exposed to the strong central radiation accelerating the motion. The nonlocal clouds, if present, actually fall onto the entire disk surface and could interact with the local population. Nevertheless, our simple model does not account for this possibility.

The parameters of the cloud collision with the disk are calculated by comparing the ram pressure exerted by the cloud with the local pressure inside the disk. The ram pressure of the cloud is calculated from the formula

\[
P_{\text{ram}} = n_c m_p v_z^2. \tag{4}
\]

The velocity \( v_z \) is calculated in the local frame co-moving with the disk, i.e., the local Keplerian speed is subtracted. The disk height and the disk vertical structure needed to estimate the depth of the cloud penetration are calculated as in Różański et al. (1999) and Czerny et al. (2016), but without introducing the hot corona or self-gravity to the disk structure (Shlosman & Begelman 1989; Karas et al. 2004). All other effects are included, i.e., the proper description of the opacity, including the dust and molecules (see the description in Naddaf et al. 2021), convection, and gas and radiation pressure. With the pressure profile inside the disk obtained, \( P \equiv P(z) \), we compute...
the impact depth from the condition
\[ P_{\text{ram}} = P(z_{\text{impact}}), \] (5)
where we introduce the local density and the temperature from the disk structure. Computations are performed at the radius corresponding to the cloud impact position, neglecting the deceleration of the cloud across the disk as well as the change of its distance from the center when passing through the disk interior. The viscosity parameter \( \alpha_{\text{acc}} \) introduced by Shakura & Sunyaev (1973) is assumed to be 0.02, as estimated at the basis of variability (see Grzédzielski et al. 2017, and the references therein).

We find that clouds in models adopting the solar metallicity are stopped by the disk, usually relatively close to the disk surface. However, for high-metallicity models, the condition given in Equation (5) is never met, because the ram pressure of some clouds is higher than the equatorial disk pressure. This means that such clouds should traverse the disk and reappear on the other side. In this case, we use the equatorial values to characterize the disk density and calculate the shock conditions in the next section.

2.4. Shock Properties and Nonthermal Emission

The supersonic collision of a BLR cloud with the accretion disk produces a forward shock in the disk and a reverse shock in the cloud. The velocities of these shocks can be calculated as (see e.g., Tenorio-Tagle 1981; Lee et al. 1996)
\[ U_{\text{cloud}} = -\frac{4}{3} \frac{v_{\text{impact}}}{1+a}, \quad U_{\text{disk}} = \frac{4}{3} \frac{v_{\text{impact}}}{1+a} \] (6)
where \( v_{\text{impact}} \) is the impact velocity of the cloud, \( a = \sqrt{n_{\text{cloud}}/n_{\text{disk}}} \), and \( n_{\text{disk}} \) is the disk density at the impact radius. Müller & Romero (2020) assumed the impact velocity equal to the Keplerian orbital velocity, while the value adopted in this work is calculated as the vertical component predicted by the FRADO model, which results in only a fraction of the Keplerian speed.

The characteristic timescale of the system is defined by the time required by the shock to cross the cloud. This assumption is true if the cloud has not been previously destroyed by hydrodynamic instabilities or another process. Indeed, some authors have suggested that the BLR clouds have lifetimes of only a few months (Maiolino et al. 2010; Ramos Almeida & Ricci 2017). Nevertheless, these estimates consider that the clouds do not possess magnetic fields and their surrounding medium is stationary. Because clouds in the FRADO model are created from the accretion disk, it is more appropriate to think that they should be magnetized objects and therefore survive longer (Shin et al. 2008). We present a more detailed discussion about the stability of the clouds in the Appendix.

Shocks that are strong, adiabatic, and super-Alfvénic can accelerate particles efficiently up to relativistic energies by the diffusive shock acceleration (DSA) mechanism (Bell 1978; Blandford & Ostriker 1978). In the case of parallel shocks and diffusion in the Bohm regime, the acceleration time for electrons and protons with energies \( E_{e,p} \) in a magnetic field \( B \) is (Drury 1983; Protheroe 1999)
\[ t_{\text{acc}} \sim 2.4 \times 10^9 \left( \frac{E_{e,p}}{\text{TeV}} \right) \frac{B}{G} \left( \frac{v_{sh}}{100 \text{ km s}^{-1}} \right)^{-2}. \] (7)
Given the lack of direct information of the value of \( B \) in these regions, we consider a sub-equipartition relation between the magnetic energy density and the ram pressure of the shocked cloud gas
\[ \frac{B^2}{8\pi} = \frac{9}{8} \frac{m_p n_e v_{sh}^2}{\beta}, \] (8)
where \( \beta \leq 1 \) is the magnetization parameter. We obtain
\[ \frac{B}{G} \sim 22 \left( \frac{\beta}{0.1} \right)^{\frac{1}{2}} \left( \frac{n_e}{10^{12} \text{ cm}^{-3}} \right)^{\frac{1}{2}} \left( \frac{v_{sh}}{100 \text{ km s}^{-1}} \right). \] (9)
If we adopt a conservative value of \( \beta = 0.1 \), the typical magnetic field deduced for the inner clouds of the BLR is of hundreds of Gauss. The estimated value becomes of the same order of magnitude assuming that the magnetic field is in sub-equipartition with the kinetic energy of the collision.

Particles escape from the acceleration region typically by diffusion, with timescale
\[ t_{\text{diff}} \sim 5.1 \times 10^9 \left( \frac{R_c}{10^{12} \text{ cm}} \right)^2 \left( \frac{E_{e,p}}{\text{TeV}} \right)^{-1} \left( \frac{B}{G} \right). \] (10)
in the Bohm diffusion regime. The adiabatic expansion of the perturbed cloud gas also decreases the energy of the particles, so that
\[ t_{\text{ad}} \sim 5 \times 10^9 \left( \frac{R_c}{10^{12} \text{ cm}} \right) \left( \frac{v_{sh}}{100 \text{ km s}^{-1}} \right)^{-1}. \] (11)
The most relevant cooling mechanism for the electrons is the synchrotron one (see Figure 2), operating at the timescale
\[ t_{\text{synch}} \sim 4 \times 10^9 \left( \frac{E_e}{\text{TeV}} \right)^{-1} \left( \frac{B}{G} \right)^{-2}. \] (12)
By equating \( t_{\text{acc}} = t_{\text{synch}} \), we find that the electrons' maximum energy constrained by synchrotron cooling is
\[ E_{e,\text{max}} \sim 17 \left( \frac{B}{G} \right)^{\frac{1}{2}} \left( \frac{v_{sh}}{100 \text{ km s}^{-1}} \right). \] (13)

The interaction of the electrons with the surrounding matter leads to relativistic bremsstrahlung, whose characteristic
timescale is given by

$$t_{\text{pp}}/s \sim 2 \times 10^3 \left( \frac{n_c}{10^{12} \text{ cm}^{-3}} \right)^{-1}.$$  

(14)

Target photons for inverse Compton (IC) scattering are provided by the BLR and the accretion disk, with energy densities $U_{\text{BLR}} = 0.1 L_{\text{disk}}/(\pi R_{\text{BLR}}^2 c)$ and $U_{\text{disk}} = 4 \sigma_b T_{\text{disk}}^4/c$, respectively (see Table 2). For computing the IC cooling rate and the emissivity, we follow the calculations presented by Aharonian & Atoyan (1981). The BLR and accretion disk photon fields are also taken into account for calculating the absorption of gamma emission and the injection of secondary particles (Müller & Romero 2020).

Protons are expected to interact with the local dense medium and lose energy due to proton-proton (PP) inelastic collisions on a timescale

$$t_{\text{pp}}/s \sim 2 \times 10^3 \left( \frac{n_c}{10^{12} \text{ cm}^{-3}} \right)^{-1}.$$  

(15)

In Figure 3, we plot the relevant timescales for protons. We find that the maximum energy that protons can get is $E_{p,\text{max}} \approx \text{TeV}$, and it is determined by the lifetime of the adiabatic shock.

We solve numerically the kinetic equation

$$\frac{\partial N_{e,p}(E, t)}{\partial t} + \frac{\partial [b(E)N_{e,p}(E, t)]}{\partial E} + \frac{N_{e,p}(E, t)}{t_{\text{esc}}(E)} = Q_{e,p}(E)$$  

(16)

to find the energy distribution of electrons ($N_{e}$) and protons ($N_{p}$). In Equation (16), $Q_{e,p} \propto E_{e,p}^2$ is the injection rate of particles, $b(E) = E/t_{\text{cool}}(E)$ accounts vice versa for the energy losses, and $t_{\text{esc}}(E) = t_{\text{diff}}(E)$. The luminosity due to injected relativistic particles is assumed to be 0.1 $L_{e}$, where $L_{e} = \frac{1}{2} M_{\text{V}} v_{\text{impact}}^2/t_{\text{coll}}$ is the power released during the collision (del Valle et al. 2018). Additionally, we consider this energy equally distributed between electrons and protons ($L_{p}/L_{e} = 1$), as well as the case with a hundred times more energy in protons than electrons ($L_{p}/L_{e} = 100$). The lepto-hadronic spectral energy distribution (SED) is finally calculated using the expressions referred in Müller & Romero (2020).

### Figure 3

Idem to Figure 2, but for protons.

### Figure 4

Density profiles of the unshocked disk and the unshocked cloud assuming $Z = 5 Z_{\odot}$, $M_{\text{BH}} = 10^8$ (solid lines) and $10^6$ $M_{\odot}$ (dashed lines); and $m = 0.01$ (blue), 0.1 (green), and 1.0 (red). The dark colors correspond to the local population of clouds, and the light colors are the nonlocal ones. The impact positions are normalized to the size of the BLR in each case, i.e., 0 is the position of BLR inner boundary $R_{\text{in}}$, while 1 is the outer radius $R_{\text{out}}$. The orange solid line indicates the density of the clouds, in this case fixed to $10^7$ cm$^{-3}$.

### 3. Results

The efficiency of the production of nonthermal radiation from the shocks depends on the specific model parameters. The black hole mass, accretion rate, and metallicity directly affect the impact velocities of the clouds in the FRADO model, and subsequently, the shock properties. As a reference model, we use the solution with expected high nonthermal emission: $M_{\text{BH}} = 10^8 M_{\odot}$, $m = 1$, and super-solar metallicity $Z = 5 Z_{\odot}$, and we show the dependence of the results on these parameters.

#### 3.1. The Distribution of the Impact Properties and Shock Waves

Equation (6) shows that the shock speed depends not only on the vertical component of the cloud velocity, but also of the cloud and disk densities. While the cloud density is fixed to $10^{11-12}$ cm$^{-3}$, the local density of the accretion disk is a function of $M_{\text{BH}}$, $m$, $Z$, and the penetration depth of the cloud. In Figure 4, we display the density of the accretion disk at the location of the impact for the different parameter sets explored in this work. For a high black hole mass, the clouds penetrate much deeper into the disk, where the densities are higher, some of them reaching the equatorial plane. Such clouds, as mentioned in Section 2.2, may cross the disk and even reappear on the other side. Nevertheless, because the crossing time of the clouds is much longer than the characteristic timescale of the system, we assume that in such cases the disk equatorial density determines the shock parameters. For small
black hole mass the clouds are stopped very close to the disk surface. The dependence on the accretion rate is complex because both the clouds' velocities and the disk internal structure depend on this parameter.

The impact velocity of the clouds ($v_{\text{impact}}$) and the associated shocks speeds ($U_{\text{disk}}$, $U_{\text{cloud}}$) are shown in Figure 5. The impact velocity of the clouds increases with the accretion rate, the black hole mass, and the metallicity. In the very low accretion regime, i.e., $\dot{m} = 0.01$ (blue), 0.1 (green), and 1.0 (red). The dotted lines show the velocity of the reverse shocks, whereas the dashed lines denote the velocity of the forward shocks. The dark colors are the local population of clouds, and the light colors the nonlocal. The impact positions are normalized to the size of the BLR.

![Figure 5](image1.png)

**Figure 5.** Impact (solid lines) and shock velocities assuming $Z = 5 Z_{\odot}$, $M_{\text{BH}} = 10^8$ (top panel) and $10^6$ $M_{\odot}$ (bottom panel); and $\dot{m} = 0.01$ (blue), 0.1 (green), and 1.0 (red). The dotted lines show the velocity of the reverse shocks, whereas the dashed lines denote the velocity of the forward shocks. The dark colors are the local population of clouds, and the light colors the nonlocal. The impact positions are normalized to the size of the BLR.

3.2. Spectral Energy Distributions

In Figure 6 we plot the SED for the particular case with $Z = 5 Z_{\odot}$, $M_{\text{BH}} = 10^8$ $M_{\odot}$, $\dot{m} = 1$, $n_c = 10^{12}$ cm$^{-3}$, $R_c = 10^{12}$ cm, and a ratio of energy injected in protons to electrons $L_p/L_e = 100$. The black line shows the total BLR emission, whereas the other lines represent the contribution from the innermost ring of clouds.

![Figure 6](image2.png)

**Figure 6.** Spectral energy distribution for electrons and protons in a special case of $Z = 5 Z_{\odot}$, $M_{\text{BH}} = 10^8$ $M_{\odot}$, $\dot{m} = 1$, $n_c = 10^{12}$ cm$^{-3}$, $R_c = 10^{12}$ cm, and a ratio of energy injected in protons to electrons $L_p/L_e = 100$. The black line shows the total BLR emission, whereas the other lines represent the contribution from the innermost ring of clouds.

In all the cases, the mass of the supermassive BH is $10^8$ $M_{\odot}$.

![Figure 7](image3.png)

**Figure 7.** Spectral energy distribution for different parameter sets. In all the cases, the mass of the supermassive BH is $10^8$ $M_{\odot}$.

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luminosities but not in the shape of the SED. This is because the velocity of the shock wave in the less dense medium increases and the lifetime of the adiabatic shock is prolonged as well. Therefore, the fraction of the energy released in the impact that can be injected in relativistic particles rises. Thus, the velocity of the shock wave in the less dense medium is assumed to be twice its vertical component, the maximum impact velocity, or change the cloud density predicts a 2 keV luminosity of $10^{44}$ erg s$^{-1}$ as shown in Figure 8.

As we mentioned before, considering the impact velocity equal to the vertical velocity component produces a drop in the spectra at MeV. In Figure 8, we show how the results change if we duplicate the effective impact velocity, or change the cloud density predicts a 2 keV luminosity of $10^{44}$ erg s$^{-1}$ as shown in Figure 8.

Figure 8. Spectral energy distribution for different parameter sets. The model with $Z = 5 Z_{\odot}$, $M_{\text{BH}} = 10^8 M_{\odot}$, $m = 1$, $R_c = 10^{13}$ cm, $n_i = 10^{13}$ cm$^{-3}$, and $L_p/L_c = 100$ is plotted as the reference model.

3.3. Comparison of the Predicted X-Ray Nonthermal Flux with the Data for AGNs

A simple analysis of the predicted role of the nonthermal emission in non-jetted sources can be done on the basis of the observed UV/X-ray statistical trend (Lusso & Risaliti 2016). Fits to the UV flux measured at 2500 A($L_{\text{UV}}$) and 2 keV ($L_X$) give a nonlinear relation between the two

$$\log L_X = 27.46 + 0.53 \log L_{\text{UV}}, \quad (17)$$

where the exact values were taken from Salvestrini et al. (2019). Our model shown in Figure 7 has the bolometric luminosity of $\sim 10^{46}$ erg s$^{-1}$. Using the bolometric correction of 27 to obtain the 2 keV flux, we expect the X-ray flux there at a level of $4 \times 10^{43}$ erg s$^{-1}$. The model with a high cloud density predicts the flux there to be $\sim 10^{44}$ erg s$^{-1}$, suggesting a few percent contribution to the total X-ray flux. However, the low cloud density predicts a 2 keV flux of $\sim 10^{43}$ erg s$^{-1}$, which combined with a higher effective impact velocity could lead to a 2 keV luminosity of $10^{44}$ erg s$^{-1}$ as shown in Figure 8.

Laor & Behar (2008) have found that, in radio-quiet AGNs, the luminosity at 5 GHz and the integrated X-ray luminosity ranging from 0.2 to 20 keV follows the relation $L_{5\text{GHz}}/L_{0.2-20\text{keV}} \sim 10^{-3}$. The exact SED shape of our models in the low-energy radio domain depends on the accretion rate as well as the ratio $L_{\text{p}}/L_c$. In cases with higher X-ray emission, i.e., $M = 10^8 M_{\odot}$, $Z = 5 Z_{\odot}$, $n_i = 10^{13}$ cm$^{-3}$, and $L_p/L_c = 100$ (see Figures 7 and 8), we find that $L_{5\text{GHz}}/L_{0.2-20\text{keV}} \sim 10^{-2}$ as a consequence of the synchrotron self-absorbed emission at frequencies below $10$ GHz. This result indicates that if the interaction of BLR clouds with the accretion disk contributes significantly to the X-ray band, an additional source emitting at 5 GHz is needed to match the trend observed by Laor & Behar (2008). Behar et al. (2015, 2018) evaluate an analogous relation using a higher radio frequency. Their study indicates that $L_{5\text{GHz}}/L_{2-10\text{keV}} = 10^{-4}$. In our case, we find that $L_{5\text{GHz}}/L_{2-10\text{keV}} \approx 1.5 \times 10^{-4}$. This shows that the nonthermal emission has a potential to contribute to the observed X-ray flux in non-jetted sources, but the model predictions are extremely sensitive to the adopted cloud density. Therefore, future comparison with the observational data has to concentrate more on the specific shape of the broadband X-ray spectrum.

We stress that while we consider a contribution of the nonthermal emission to X-ray spectra, we do not claim that nonthermal emission produced via cloud-disk interactions is the sole mechanism of X-ray radiation in radio-quiet sources, because that would contradict the presence of the relativistic Compton reflection, relativistically broadened iron Kα line, and all energy-resolved time delay studies (e.g., Pounds et al. 1990; Reynolds et al. 1999; Dovčiak et al. 2004; Karas et al. 2021, 2022).

In particular, this model cannot reproduce the characteristic short-scale X-ray variability observed in AGNs. The stochastic variability level in our model is low, because the total number of clouds in BLR is high, and even the number of impacts per second is of order of 6000 for a model with 5 $Z_{\odot}$, $M_{\text{BH}} = 10^8 M_{\odot}$, and $m = 1$, which implies a variability level of 1%. However, the variations of the accretion rate in the innermost part of the flow can be very fast, as inferred from studies of some changing-look AGNs (e.g., Liang et al. 2022). Such a sudden change of the bolometric luminosity affects the
motion of the clouds high above the disk and modifies the impact radii and velocities. In addition, observations of stellar winds in supergiant stars clearly show that wind launching is episodic (e.g., Humphreys & Jones 2022). Such a type of outflow behavior can additionally enhance the level of variability.

3.4. Comparison of the Predicted Gamma-Ray Flux with the Data for AGNs

Despite the fact that AGNs make up at least 80% of the gamma-ray resolved sources, the number of identified GeV radio-quiet/radio-weak objects is just a few tens (Abdollahi et al. 2020). For this reason, a relation similar to Equation (17) has not been established yet, although some authors have already suggested that the gamma emission seems to correlate with the X-ray radiation, and therefore with the properties of the AGN (Wojaczyński et al. 2015; Wojaczyński & Niedźwiecki 2017). Within the group of potential weak-jetted gamma-ray AGNs, there is one particular kind of object that has been growing in popularity and number: the so-called narrow-line Seyfert 1 galaxies (NLSy1s; Paliya 2019). The peculiar spectra of these galaxies show the broad-emission lines observed in Seyfert 1 galaxies, but narrower, and also a steep gamma-ray fall similar to flat-spectrum radio quasars. Therefore, it has been proposed that they represent an intermediate state between these two AGN classes. Because Seyfert galaxies are high-accreting objects, they become natural candidates for the model presented in this work. As we showed, the efficiency of the production of the nonthermal emission by the collisions of BLR clouds increases with the accretion rate. In Müller & Romero (2020), the authors have already found that if the energy transmitted to the production of the shock waves corresponds to the Keplerian velocity of the clouds, the model explains successfully the gamma emission from the nearby Seyfert galaxy NGC 1068. Nevertheless, the detection of more distant galaxies is very challenging because of the sensitivity of the current gamma-ray instruments.

The observational information of NLSy1s seems to indicate that the gamma-emitter objects are radio-loud sources containing a pc-scale jet with Doppler factors of 5–10, and that therefore the GeV radiation is typically associated with the existence of a jet. A rather indirect argument for a jet-powered nonthermal radio emission comes from the first detection of the fast (day) variability in NLSy1 Mrk 110 (Panessa et al. 2022); however, the compactness of the region is inferred from the timescale, although it might reflect a turbulence at somewhat larger radii. In any case, the radio and gamma-ray emission do not need to have the same origin. Additionally, not all the radio-loud NLSy1s have been detected at gamma-ray energies.

Paliya et al. (2019) compiled the data of all the discovered gamma NLSy1s, which total only 16 (only nine of them are bona fide sources, according to D’Ammando 2019). The authors found that the fit of the SEDs requires the assumption that the contribution of the components is not the same in every source, e.g., the X-ray radiation is sometimes explained by a corona and synchrotron self-Compton radiation and other times by the Compton up-scattering of external photons. On the other hand, the gamma-ray emission is always explained by inverse Compton, but sometimes with photons from the BLR and other times from the dusty torus. Moreover, GeV blazar-like flares of four gamma NLSy1s have been reported over the last years (Gokus et al. 2021). Some of the flares are simultaneously observed in soft X-ray and gamma rays, but not all of them, and non-hard X-ray variations have been detected, suggesting that there should exist several emission regions (Paliya 2019). In particular, SBS 0846+513 and PKS 1502+036 have been observed in gamma rays during the low state without showing any coincidence with superluminal motion in radio. In the case of SBS 0846+513, superluminal motion has also been measured without an associated gamma-ray flare. Furthermore, the low- and high-activity SEDs can be modeled as synchrotron and external Compton radiation, but the transition between both states requires not only a change in the electron distribution of the emitting region, but also a change in the magnetic field value (D’Ammando 2019). This can also be interpreted as a different radiative region dominating the gamma emission during the different states, as observed in the X-ray band of some NLSy1s, where the corona prevails during the low gamma-ray activity and the jet during the gamma-ray flares (Paliya 2019).

The model presented in this work does not aim to explain flaring episodes of a few hours, which are likely related to the presence of a relativistic outflow, but it could significantly contribute to the continuous and/or long-variable emission from NLSy1s. During the flares, electrons accelerated in the jet might dominate the gamma rays produced by external Compton scattering of photons, whereas in the low states, the radiation could mainly be provided by other components, e.g., the collisions in the BLR. As indicated in Figure 8, the luminosity expected from our model rises with the mass of the central BH and the accretion rate. Therefore, gamma rays of distant NLSy1s with typical black holes of $10^8 M_\odot$ are detected, in contrast to nearby Seyfert galaxies with typical masses of $10^6 M_\odot$. In addition, our model can reproduce the photon index of $\sim 1.6$ that is commonly observed at hard X-ray energies (Paliya 2019) and offers a hadronic contribution to the gamma emission of NLSy1s, which leaves open the possibility of neutrino production.

In radio-quiet AGNs as well as quiescent galactic nuclei such as the Galactic center, another potential source of long-term gamma-ray emission is a population of old millisecond pulsars. It is expected that there is a substantial population of neutron stars of various ages in the dense nuclear star clusters (NSCs), such as inside the NSC in the Galactic center, which has been studied in detail (Zajaček et al. 2015; Eckart et al. 2017; Karas et al. 2017; Zajaček et al. 2017). In particular, the subpopulation of old, accretion-powered millisecond pulsars could be a source of the extended and diffuse gamma-ray emission as analyzed by Wang et al. (2005) and recently by Gautam et al. (2021). In this scenario, the gamma rays are produced by the prompt emission of electron-positron pairs in the millisecond pulsar magnetospheres and also by the delayed emission of the escaping pairs in the pulsar wind shocks via the inverse Compton scattering on the interstellar radiation field. In both cases, the gamma-ray emission originates in the rotational kinetic energy of the pulsars at the age of $\sim 13.8$ Gyr via the magnetic dipole braking. The model has been successful in explaining the Galactic center gamma-ray excess (Gautam et al. 2021). The peak luminosity that possibly originates from a millisecond pulsar population is $L_{\text{MSp}} \approx 4 \times 10^{46} \text{ erg s}^{-1}$ (see Figure 3 in Gautam et al. 2021), which is two orders of magnitude smaller in comparison to the nonthermal GeV luminosity from cloud-disk collisions (for $10^8 M_\odot$ BH, see Figure 8 in this paper, where the GeV luminosity is

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Figure 9. The ratio of the local accretion rate to the initially adopted disk accretion rate for the most extreme case with initial parameters of $M_{\text{BH}} = 10^5 M_\odot$, $Z = 5 Z_\odot$, $m = 1$, and $n_e = 10^{11} \text{ cm}^{-3}$. The local accretion rate was calculated by solving the continuity equation, including local net effect of the infall and outflow of the clouds from the disk surface. Inflow dominates at large radii, so the net accretion rate rises initially toward smaller radii, reaches the maximum at $12,023 r_g$ (marked by the blue dotted line), and later returns to the initial value due to outflow. This effect is not included in the disk computations. \( \sim 10^{38} \text{ erg s}^{-1} \). Hence the GeV emission of millisecond pulsars, in case they are present in radio-quiet AGNs, is not expected to preclude the detection of the BLR nonthermal GeV emission.

3.5. Model Self-consistent Accretion Rate

In this work, we consider that the accretion rate is constant along the accretion disk in order to save computing time. Nevertheless, the stream of matter created by the infalling and outflowing clouds can lead to local variations of the accretion rate along the accretion disk radius. In Figure 9, we display an estimation of the net accretion rate, taking into account the outflow/inflow of clouds for the model parameters corresponding to the most efficient production of nonthermal emission. This result shows that the stream of matter produces a local rise of the accretion rate along the BLR length. For a system with $M_{\text{BH}} = 10^5 M_\odot$, $Z = 5 Z_\odot$, $m = 1$, and $n_e = 10^{11} \text{ cm}^{-3}$, we find a maximum at $r \approx 1.2 \times 10^4 r_g$, where the accretion rate reaches a value two orders of magnitude above the model value. Accounting for this effect requires performing iterative calculations of the disk structure and the BLR dynamics, which is beyond the scope of this paper, but which should be implemented in the future. The outcome of such computations is not simple to evaluate. Much larger accretion rates in the efficient impact zone would imply still higher outflow and inflow rates, as can be inferred from Equation (3). However, the effective temperature in the involved region rises in this case above the sublimation temperature of the dust, which actually would turn off the outflow completely in the zone, moving the outflow zone outwards. A stationary solution could form, with the outflow zone slightly more distant than in the model without the self-consistency requirement satisfied. In that case, the outflow would be less vigorous, because the central flux available for the material high above the disk will not be enhanced (inner accretion rate is fixed) and may be slightly suppressed due to the somewhat larger distance of the launching zone. The locally enhanced continuum emission will contribute to the near-IR and may actually mimic the warm dust component in the spectrum. On the other hand, a nonstationary solution could lead to an oscillating position of the outflow zone, which may produce time-dependent behaviors in the spectrum.

4. Summary and Conclusions

In this paper, we expand the study by Müller & Romero (2020) of the nonthermal emission arising from BLR cloud impacts onto the accretion disk, adopting the FRADO model for a detailed description of the clouds’ motion and computing the accretion disk internal density distribution. In this model, clouds are launched initially by the local radiation density field, but they are accelerated afterward by the nonlocal radiation coming from the unshielded part of the accretion disk. Cloud velocities are thus much higher than expected just from the locally available energy dissipated in the accretion disk and available as radiation flux, but their vertical components are nevertheless lower than the Keplerian velocities adopted by Müller & Romero (2020).

We show that reduced impact velocities in comparison with the original work lead to an efficient production of nonthermal emission, but only for a fraction of the parameter space. The assumption of solar metallicity of the material does not lead to impact velocities large enough to produce nonthermal emission efficiently. Nevertheless, considering the metallicity five times higher enhances the predicted flux by two orders of magnitude. This fact agrees with the results of Naddaf et al. (2021) and Naddaf & Czerny (2021), where more powerful outflows are produced at higher metallicities. This implies that in case there is nonthermal emission associated with the dynamics of the BLR, the metallicity and the intensity of the radiation will be linked. The second key parameter of the model is the cloud density. Denser cloud models ($n_e \sim 10^{12} \text{ cm}^{-3}$) under-predict the expected X-ray luminosity at 2 keV in non-jetted AGNs by several orders of magnitude, while lower-density clouds ($n_e \sim 10^{11} \text{ cm}^{-3}$) could contribute to the X-ray emission. Interestingly, not only the luminosity but also the shape of the nonthermal emission depends on the Eddington rate of the source, which manifests that the intrinsic properties of the AGN are imprinted in the radiation. If the energy fraction released in the impact is at least twice the fraction of the kinetic energy calculated using only the vertical component of the velocity computed with the FRADO model, the SEDs present some similarities to the ones observed in gamma NLSy1s. Nevertheless, determining precisely the effective impact velocities will require detailed magnetohydrodynamic studies. In all the cases, the spectra show pronounced differences in the MeV range.

Our model predicting the cloud-disk interaction is based on the assumption that clouds are launched and accelerated solely by the radiation pressure acting on dust. However, higher above the disk, the line-driving mechanism certainly contributes to the acceleration as well, and the final cloud velocities might be larger. At present, we cannot calculate quantitatively the combined effect of the radiation and line-driving mechanisms, because this is a very complicated computational problem. However, in the future, the dust-based code should be combined with line-driving codes, such as QWIND (Risaliti & Elvis 2010; Quera-Bofarull et al. 2021).

The non-hydrodynamical models use the concept of clouds instead of a continuous wind. In reality, the outflow is probably launched as a roughly uniform wind, and later instabilities lead...
both to formation of the clouds embedded in the intercloud (almost co-moving) medium, and multiple processes work toward cloud condensation and cloud destruction. These processes are observed in stellar winds. We discuss these unresolved issues extensively in the Appendix.

The scenario of cloud-disk interaction presented in this paper could be enriched by considering additional processes. For instance, the bow shocks created by the clouds moving with Keplerian velocities through the surrounding medium could also accelerate particles and be an extra source of nonthermal emission. On the other hand, complete dynamical models such as FRADO can provide the statistics of clouds that escape and do not collide with the disk. This can be employed to estimate the probability of clouds that enter jets in jetted systems (see e.g., Dar & Laor 1997; Araudo et al. 2010; del Palacio et al. 2019). In addition, considering BLR models that describe the photon field at each point inside these regions can improve the nonthermal emission and absorption maps at the highest energies. Therefore, the observations performed by the next generation of MeV and gamma observatories, such as AMEGO or AMEGO-X and the Cherenkov Telescope Array, will contribute substantially to these studies (McEnery et al. 2019; CTA Consortium & Ong 2019).

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Appendix

Cloud Formation and Destruction, Shock Formation Mechanisms

The presented scenario of nonthermal emission is based on the assumption of the cloud formation soon after the wind is launched, and cloud survival until the moment of the impact onto the disk surface. The formation and existence of the two-phase medium at a BLR distance is a difficult topic, although the possibility of the thermal instabilities in the irradiated environment in AGNs was already considered several decades ago (Krolik et al. 1981; Begelman & McKee 1990a; Różyńska & Czerny 2000). However, the stability of cloud structures close to galactic nuclei, despite tens of years of observational, analytical, and numerical studies, is still a matter of debate due to the presence of external pressure and the tidal field, among other factors (Chen et al. 2016). Therefore, we examine the aspect of the BLR cloud formation and its stability during the expected flight time within the FRADO model below in some detail.

A.1. BLR Cloud Thermal Stability

The inner gravitational radii where the BLR clouds originate are characterized by a multiphase medium. The low-ionization BLR clouds are dense structures with $n_c \sim 10^{12}$ cm$^{-3}$, whereas the typical disk densities are $n_{\text{disk}} \sim 10^{14} - 10^{15}$ cm$^{-3}$ (see Figure 4), where we considered a standard thin disk with $m = 1$, $M_{\text{BH}} = 10^6 M_\odot$, and the BLR range of $r = 5000 - 20,000 r_g$ according to the calculations by Naddaf et al. (2021). The BLR clouds are lifted from the accretion disk into the hot intercloud medium, where we assume they are approximately in pressure equilibrium.

The BLR gas temperature is $T_c \approx 10^4$ K based on the heating/cooling balance due to atomic transitions in the partially ionized plasma (Peterson 2006; Czerny 2019). The intercloud medium is kept close to the Compton limit of a few $\sim 10^7$ K due to heating/cooling by the Compton scattering (Krolik et al. 1981). The irradiation by the intense hard central source is expected to lead to the development of the thermal instability and the two phases above the disk plane coexist with the number density ratio of $n_c/n_h \sim 10^3$, where $n_h \sim n_c T_c/T_h \sim 10^9$ cm$^{-3}$ is the number density of the hot medium inferred from the assumed pressure equilibrium.

First, we consider the motion of a BLR cloud through a hot, stationary plasma. In that case, the ablation of the cloud likely takes place due to its interception by the hot plasma with a certain velocity difference. The mass-loss rate of the cloud then can be expressed as (Kwak et al. 2011; Burkert et al. 2012),

$$\frac{dM_c}{dt} \approx -q_{abl} \pi R^2_c m_p n_h v_c,$$ (A1)

where $v_c$ is the cloud velocity with the dominant Keplerian component at the launch radius and $q_{abl}$ is the ablation coefficient. Assuming that $n_c$ is constant, the cloud radius evolution is

$$\frac{dR_c}{dt} = -\frac{q_{abl} v_c}{4} \rho_h \rho_c$$ (A2)

and the ablation timescale is

$$\tau_{abl} \approx \frac{4R_c}{q_{abl} v_c \rho_h} \approx 106 \left(\frac{R_c}{10^{12} \text{ cm}}\right)^{-1} \left(\frac{v_c}{3000 \text{ km s}^{-1}}\right)^{-1} \left(\frac{\rho_c}{10^3 \text{ g cm}^{-3}}\right) \text{yr},$$ (A3)

where we fixed $q_{abl} = 0.004$ (Kwak et al. 2011).

A small BLR cloud surrounded by the hot medium also loses mass and evaporates due to the thermal conduction. The thermal conduction can be treated in a classical diffusion approximation because the saturation parameter (Cowie & McKee 1977)

$$\sigma_0 \approx 1.84 \frac{\lambda_{el}}{R_c} \approx 10^{-9} \left(\frac{T_h}{10^9 \text{ K}}\right) \left(\frac{R_c}{10^{12} \text{ cm}}\right)^{-1} \left(\frac{n_h}{10^9 \text{ cm}^{-3}}\right)^{-1},$$ (A4)

where $\lambda_{el}$ is the electron mean-free path, is smaller than one. Using the classical diffusion approximation below the saturation level, the evaporation timescale can be estimated as
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Figure 10. Flight time of BLR clouds as a function of the launch Keplerian velocity for $M_{\text{BH}} = 10^8 M_\odot$, $\dot{m} = 1$, and two shielding parameter values ($\alpha = 3$ and 5). The ablation, evaporation, Kelvin–Helmholtz, tidal, dynamical, and condensation timescales are shown by lines according to the legend. The top x-axis is the launch radius in gravitational radii.

\begin{equation}
\tau_{\text{evap}} \sim 110 \left( \frac{n_c}{10^{12} \text{ cm}^{-3}} \right) \left( \frac{R_c}{10^{12} \text{ cm}} \right)^2 
\times \left( \frac{T_h}{10^5 \text{ K}} \right)^{-2} \left( \frac{\log \Lambda}{30} \right) \text{ yr}, \tag{A5}
\end{equation}

where $\log \Lambda$ is the Coulomb logarithm.

Due to the velocity shear $v_{\text{shear}}$ between the BLR clouds and the hot medium, or the shock created in a supersonic motion, which can be estimated to be equal to the initial launch Keplerian velocity $v_k$, the clumps are subject to Kelvin–Helmholtz (KH) instabilities with the characteristic size of $\lambda_{\text{KH}} \sim R_c$. Given the density ratio between the medium and the clouds, $r_\rho = n_h/n_c \sim 10^{-3}$, the characteristic timescale $\tau_{\text{KH}}$ for the growth of instabilities of the size $\lambda_{\text{KH}} \sim R_c$ can be calculated as (see e.g., McCourt et al. 2015; Peißker et al. 2020)

\begin{align}
\tau_{\text{KH}} &= \frac{\lambda_{\text{KH}}}{v_{\text{shear}}} \sqrt{r_\rho} \\
&= 3.3 \times 10^{-3} \left( \frac{\lambda_{\text{KH}}}{10^{12} \text{ cm}} \right) \left( \frac{v_{\text{shear}}}{3000 \text{ km s}^{-1}} \right)^{-1} \\
&\times \frac{1 + r_\rho}{\sqrt{r_\rho}} \text{ yr} \sim 1.2 \text{ days}. \tag{A6}
\end{align}

The dynamical timescale, on which any perturbation inside the cloud propagates, is

\begin{equation}
\tau_{\text{dyn}} = \frac{R_c}{c_c} = 0.025 \left( \frac{R_c}{10^{12} \text{ cm}} \right) \left( \frac{\mu}{0.5} \right) \left( \frac{T_c}{10^4 \text{ K}} \right)^{1/2} \text{ yr} \tag{A7}
\end{equation}

where $c_c$ denotes the sound speed inside the BLR cloud and we adopted the mean molecular weight of $\mu = 0.5$ corresponding to the ionized hydrogen plasma.

In Figure 10, we plot the cloud flight time $t_{\text{flight}}$ as a function of the launch Keplerian velocity that is a dominant velocity component during the motion. For these exemplary calculations, we consider $M_{\text{BH}} = 10^8 M_\odot$, $\dot{m} = 1$, and two different shielding parameter values, $\alpha = 3$ (black points) and 5 (blue points) (Naddaf et al. 2021). For comparison, we also plot $\tau_{\text{abl}}$, $\tau_{\text{evap}}$, $\tau_{\text{KH}}$, and $\tau_{\text{dyn}}$ given in Equations (A3), (A5), (A6), and (A7), respectively. We can see that $\tau_{\text{abl}} \sim \tau_{\text{evap}}$, and in some cases they are shorter than $t_{\text{flight}}$. On the other hand, the Kelvin–Helmholtz timescale is at least four orders of magnitude shorter than $t_{\text{flight}}$. This implies that upon falling back onto the accretion disk, the clouds are expected to be diminished and deformed, and in some cases, they can be completely ablated and evaporated before their trajectories are completed. In the case of the existence of an entangled magnetic field inside the clouds, it can effectively inhibit the growth of Kelvin–Helmholtz instabilities and prolong the cloud lifetime (McCourt et al. 2015). However, the ablation as well as the evaporation are not expected to be significantly mitigated by
the internal magnetic field. The BLR clouds can further be affected significantly by the tidal forces that stem from the presence of the supermassive black hole (SMBH), which we analyze in subsection A.2. The destructive effect of the ablation and the evaporation is expected to be reversed by the condensation of the hot intercloud medium on the “seed” clouds, as we show in subsection A.3.

A.2. Tidal Deformation of Clouds

The shape and the stability of BLR clouds are also affected by the tidal forces in the vicinity of the SMBH. BLR clouds are about 10 orders of magnitude less massive than the critical Bonnor–Ebert mass for the collapse of an isothermal cloud, $M_{\text{BE}} \sim \rho_{\text{BE}} v_t^4/(\rho_\text{BE}^{1/2} G^{3/2})$, where $\rho_{\text{BE}} \approx 1.18$, $v_t$ is the thermal velocity inside an isothermal BLR cloud, and $P_{\text{ext}}$ is the external pressure, including the ram pressure. Assuming a BLR cloud of $T_c \sim 10^4$ K, which is moving at $v_c \sim 3000$ km s$^{-1}$ in a hot medium of $n_h \sim 10^9$ cm$^{-3}$ and $T_h \sim 10^7$ K, we obtain $M_c \ll M_{\text{BE}} \sim 11 M_\odot$.

The BLR clouds are likely not tidally stable along their trajectory across a range of distances (see Figure 10). We obtain the Roche critical density taking into account only the radial motion (Phinney 1989; Sanders 1998; Peiβker et al. 2020).

$$n_{\text{Roche}} \sim \frac{3M_{\text{BH}}}{2\pi \mu m_p r^3} = \frac{3c^6}{2\pi G^2 \mu m_p (r/r_g)^3} M_{\text{BH}}^2$$

$$\sim 3.5 \times 10^{13} \frac{r}{(4 \times 10^4 r_g)^3} \left(\frac{M_{\text{BH}}}{10^8 M_\odot}\right)^{-2} \text{cm}^{-3}.$$  \hspace{1cm} (A8)

Therefore, BLR clouds with $n_c \sim 10^{12}$ cm$^{-3} < n_{\text{Roche}}$ are tidally unstable. However, at distances larger by a factor of two than $10^4 r_g$, tidal stability could be reached in case the density is not reduced; hence, the stability with respect to tidal effects and the associated cloud distortion depend strongly on the distance.

Another indicator of the importance of tidal effects is the tidal radius $r_{\text{tidal}}$, which depends on the mass of the cloud as well as linearly on its size, as follows (Hills 1975; Rossi et al. 2020)

$$r_{\text{tidal}} \approx R_c \left(\frac{M_{\text{BH}}}{M_c}\right)^{1/3} \left(\frac{4}{3} \pi \mu m_p n_c\right)^{1/3} \left(\frac{M_{\text{BH}}}{10^8 M_\odot}\right)^{1/3} r_g,$$

$$\approx 2.6 \times 10^4 \left(\frac{M_{\text{BH}}}{10^8 M_\odot}\right)^{1/3} \left(\frac{n_c}{10^{12}} \text{cm}^{-3}\right)^{1/3} r_g.$$  \hspace{1cm} (A9)

which indicates that BLR clouds orbiting at distances $r \lesssim r_{\text{tidal}}$ are prone to tidal effects, specifically tidal stretching as well as compression. The acceleration acting on a BLR cloud of size $R_c$ (in the direction of the SMBH) due to the tidal field can be expressed as

$$|a_{\text{tidal}}| = 2R_c \frac{GM_{\text{BH}}}{r^3}. $$  \hspace{1cm} (A10)

which implies that the timescale on which the tidal deformation of the size $R_c$ develops is

$$\tau_{\text{tidal}} \approx \frac{2R_c}{|a_{\text{tidal}}|} = \frac{r^{3/2}}{\sqrt{G M_{\text{BH}}/r_g}} \left(\frac{r}{r_g}\right)^2 \frac{M_{\text{BH}}}{\left(10^8 M_\odot\right)^2} \text{yr}.$$  \hspace{1cm} (A11)

The BLR clouds are considered to be non-self-gravitating. Each cloud becomes significantly stretched by $R_c$ on a timescale shorter than or comparable to the orbital timescale $P_{\text{orb}}$. The characteristic tidal timescale expressed by Equation (A11) is depicted in Figure 10, where $t_{\text{flight}}$ is typically longer than $\tau_{\text{tidal}}$. For the shielding models with $\alpha = 3$ and 5, the mean ratio of the flight time to the orbital time is $\tau_{\text{flight}}/P_{\text{orb}} = 1.06 \pm 0.80$ and $1.03 \pm 0.88$, respectively. Hence, the mean flight time is of the order of the orbital timescale from the formation of the cloud until its fall back onto the disk, the tidal field can induce stretching by a factor of at least two.

We examine the tidal effects by a test-particle simulation, where we initially distribute particles in a spherical cloud with a Gaussian density distribution of FWHM size of $10^{12}$ cm, set at the expected cloud size (the corresponding width of the Gaussian is $4.3 \times 10^{11}$ cm), and a small velocity dispersion of $1$ km s$^{-1}$. The cloud as a whole orbits around the SMBH of $10^8 M_\odot$ at a distance of $10^4 r_g$ (with an orbital period of $\sim 98$ yr). In Figure 11 we show several snapshots of the cloud shape and its surface density distribution at $t = 0, 24.08$ (a quarter of the orbital period), and 49.12 yr (half of the orbital period). We see that a BLR cloud without any additional support would become more and more elongated, with a progressively decreasing surface density. Initially the cloud is spherical with a radius of $R_c \sim 0.07 r_g$ at the center of the cloud makes it more compact for the same velocity dispersion; see Figure 12. Placing a central core of mass $m_{\text{core}} = 10^{-3} M_\odot$ at the center of the cloud makes it more compact for the same velocity dispersion; see Figure 13. However, the tidal distortion still proceeds on the spatial scale comparable to a dispersion of $1$ km s$^{-1}$. The tidal (Hill) radius for a core of $m_{\text{core}} = 10^{-3} M_\odot$ is $r_{\text{Hill}} = a[4/m_{\text{core}}/(3M_{\text{BH}})]^{1/3} \sim 2.2 \times 10^{13}$ cm, which encompasses the whole BLR cloud.

Because of the tidal field, the BLR cloud will effectively stretch and lose mass to the surroundings, and its surface density will drop. In this sense, the mass loss and the cloud dissolution due to tidal stretching accompany the mass loss due to the ablation and the evaporation (see Equations (A3) and
Nevertheless, these processes appear to be swiftly compensated by condensation within the BLR region. We discuss this possibility in the following section.

A.3. Cloud Condensation

Clouds are not only a subject of destruction; they are expected to gain mass via the condensation from the hot surroundings in the thermal instability regime. The condensation or the evaporation prevail is given by the global saturation parameter $\sigma_0$, which expresses the ratio of the electron mean-free path to the cloud radius $R_c$ (Cowie & McKee 1977)

$$\sigma_0 = \frac{0.08\kappa_h T_h}{\Phi_s \rho_s c_s R_c}, \quad (A12)$$

where $\kappa_h$ is the thermal conductivity of the hot medium, $\Phi_s$ is a factor of the order of unity, and $c_s$ is the sound speed in the hot medium; see also Equation (A4) for comparison. For the conductivity, we use (Spitzer 1962)

$$\kappa_h = 1.84 \times 10^{-5} \Psi^{-5/2} \text{erg s}^{-1} \text{K}^{-1} \text{cm}^{-1}, \quad (A13)$$

Figure 11. The evolution of a simulated BLR cloud of free particles with a small velocity dispersion of $1 \text{ km s}^{-1}$ in the orbital plane. The cloud orbits the SMBH of $10^7 M_\odot$ at $10^4 r_g$. We show the color-coded distribution of the particle density at $t = 0$, 24.08, and 49.12 yr, which corresponds to the initial time, the quarter, and the half of the orbital period, respectively. The $x$ and $y$ axes scaling changes are according to the size of the tidally elongated cloud. The color axis scale also changes according to the peak surface density, which drops as the cloud is being tidally stretched due to the central potential.

Figure 12. The same as in Figure 11, but for the velocity dispersion of $10 \text{ km s}^{-1}$. Note the difference in the color scale with respect to Figure 11.

Figure 13. The same as in Figure 12, but including a central core of mass $10^{-3} M_\odot$. Note the difference in the color scale with respect to Figure 12.
where \( \ln \Psi = 29.7 + \ln(T_{e,0}/\sqrt{n_e}) \) with \( T_{e,0} \) being the electron temperature in \( 10^6 \) K and \( n_e \) the electron number density. Using Equation (A13), we obtain \( \sigma_0 \lesssim 4 \times 10^{-3} / \Phi_0 < 0.027 / \Phi_0 \), which implies that the material condenses onto the BLR cloud because the radiative cooling losses overcome the conductive heat input (Viezer & Hensler 2007).

Equivalently, the condition for the survival of the clouds can be expressed in terms of the Field length \( \lambda_F \) (Field 1965; Defouw 1970; Begelman & McKee 1999b)

\[
\lambda_F = \sqrt{\frac{n_e T_h}{\kappa_B T_h}}
\]

(A14)

where \( \kappa_B(T_h) \sim 10^{-23} \text{ erg s}^{-1} \text{ cm}^{-3} \) is the cooling function value for the hot medium temperature of \( T_h \sim 10^7 \) K. For the conductivity in the hot medium, we obtain \( \kappa_B \sim 2.7 \times 10^{11} \text{ erg s}^{-1} \text{ K}^{-1} \text{ cm}^{-1} \), using Equation (A13). Finally, according to Equation (A14), the Field length is \( \lambda_F \sim 5.2 \times 10^{11} \text{ cm} \).

Because the cloud radius is \( R_c \sim 10^{12} \text{ cm} \), the hot intercloud medium will rather condense on the cloud surface because the radiative cooling prevails over the thermal conduction (Różańska et al. 2014, 2017). The cloud size will tend to be progressively larger than \( \lambda_F \) during the flight time due to the tidal stretching, which will provide a greater area for the condensation to take place (cp. also Barai et al. 2012, where filamentary multiphase gaseous structure have been explored in a different context of black hole accretion). McCourt et al. (2018) argued that the thermal instability will always lead to the creation of the smallest possible clouds (with sizes much smaller than the Field length) in the form of a mist, but this may be related to their simplified treatment of the electron conduction and the neglected role of the magnetic field.

Here we derive, by performing a few approximations, the basic timescale for the condensation of the hot intercloud medium on the BLR cloud surface. The basic setup of the condensation is illustrated in Figure 14. The accreted mass via the condensation from the hot phase can be expressed as \( M_{\text{acc}} \approx 4\pi R_c^2 \rho_c \), from which the accretion rate follows as \( M_{\text{acc}} = 8\pi R_c^2 \lambda_F \rho_c \), where we assumed that the cloud radius changes due to the condensation and the Field length remains constant. By assuming that the accretion of the condensed matter onto the cloud surface is approximately spherical with the characteristic (thermal) sound speed in the hot medium of \( c_h \), we may also write \( M_{\text{acc}} = 4\pi R_c^2 \rho_c c_h \). By setting both expressions for \( M_{\text{acc}} \) equal to each other, we obtain

\[
\frac{R_c}{R_c} = \frac{c_h}{2\lambda_F},
\]

\[
\int_{R_c}^{R_c} dR_c' = \int_{0}^{t_{\text{cond}}} \frac{c_h}{2\lambda_F} dt,
\]

\[
\tau_{\text{cond}} = \frac{2\lambda_F}{c_h},
\]

\[
= 2 \left( \frac{\kappa_B n_p m_p}{k_B n_h^3 \lambda_h} \right)^{\frac{1}{2}} \sim 8.1 \times 10^{-4} \text{ yr} \sim 7.1 \text{ hr}.
\]

(A15)

Hence, the condensation process is exponential and the BLR cloud radius evolves with time as \( R_c = R_c(0) \exp(t / \tau_{\text{cond}}) \), with the characteristic condensation timescale \( \tau_{\text{cond}} \) that is orders of magnitude shorter than the evaporation timescale. Although the exponential condensation model derived here is rather simplistic in terms of geometry and stationarity, it shows that the condensation can swiftly restore the BLR cloud material despite the short KH instability and tidal timescales. The condensation timescale is also plotted for comparison in Figure 10 alongside the flight time and other hydrodynamical timescales.

A.4. Objects Interacting with the Accretion Disk

Let us note that shocks can also be produced in the accretion disk not only by the passages of clouds but also stars present in a dense nuclear cluster (Dyson et al. 1996). The relative velocity of these bodies with respect to the accretion disk medium can span a large interval. In the case of clouds emerging from the accretion disk, the majority of them are only weakly accelerated above the mid-plane, where they hover and eventually land back onto the disk surface at a similar radius with just a moderate component of the vertical velocity. On the other hand, there is a population of clouds that execute a more extended trajectory above the disk toward a different landing radius, where the azimuthal velocity component of the cloud is very different from the local orbital velocity of the underlying material.

In rare situations, the cloud motion can be influenced by the large-scale magnetic field twisted near the AGN jet axis. The cloud can then hit the disk surface in counter-rotation, which would further enhance the shock propagating from the impact place. The pressure-confined clouds thus make a significant difference from relatively weak tails behind stars passing across the accretion disk in the scenario described by Zurek et al. (1994) and Karas et al. (2004). As further pointed out, turbulence in the star wake can significantly enhance the amount of matter that is pulled out from the accretion disk plane and contribute to the supply for the BLR region and also the enhanced growth rate of the central black hole (Zurek et al. 1996; Miralda-Escudé & Kollmeier 2005).

Particle acceleration and the associated nonthermal emission due to stellar-wind bow shocks could be relevant for the closest galactic nucleus—the Galactic center (Quataert & Loeb 2005). Fast-moving S stars orbit the supermassive black hole with
velocities of a few thousand km s$^{-1}$ and depending on the properties of their stellar winds, the synchrotron flux could marginally be detectable in the radio and the infrared domains (Ginsburg et al. 2016; Zajaček et al. 2016). With the current instrument sensitivity in the near-infrared domain, the light curve of the S2 star is constant within the uncertainties, and any nonthermal contribution is beyond the detection level (Hosseini et al. 2020). This is consistent with the presence of the hot and diluted accretion flow in the Galactic center, which is in contrast to the optically thick and geometrically thin disks in AGNs where the BLR clouds can originate.

We assumed an overall smooth distribution of density in the disk or torus. In realistic setups, however, instabilities may lead to spatially concentrated variations within the disk plane. In places of significant dilution, the falling clouds can penetrate deeper into the medium, and in the extreme case, the clouds can even traverse the equatorial plane into the other hemisphere. Such penetrating collisions of BLR clouds are similar to star-disk collisions, and they could lead to the evolution of more material above the disk plane that could then contribute to wide-angle nuclear outflows (see e.g., Suková et al. 2021).

ORCID iDs
Ana Laura Müller https://orcid.org/0000-0002-8473-695X
Mohammad-Hassan Naddaf https://orcid.org/0000-0002-7604-9594
Michal Zajaček https://orcid.org/0000-0001-6450-1187
Božena Czerny https://orcid.org/0000-0001-5848-4333
Anabella Araudo https://orcid.org/0000-0001-7605-5786
Vladimír Karas https://orcid.org/0000-0002-7600-0459

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