Probing Multiple Electric Dipole Forbidden Optical Transitions in Highly Charged Nickel Ions

Shi-Yong Liang,1,2,7,* Ting-Xian Zhang,1,7,* Hua Guan,1,2,† Qi-Feng Lu,3 Jun Xiao,3,† Shao-Long Chen,1,2,8 Yao Huang,1,2 Yong-Hui Zhang,3 Cheng-Bin Li,1,† Ya-Ming Zou,3 Ji-Guang Li,4 Zong-Chao Yan,5,† Andrei Derevianko,6 Ming-Sheng Zhan,1 Ting-Yun Shi,1 and Ke-Lin Gao1,2,†

1State Key Laboratory of Magnetic Resonance and Atomic and Molecular Physics, Innovation Academy for Precision Measurement Science and Technology, Chinese Academy of Sciences, Wuhan 430071, China
2Key Laboratory of Atomic Frequency Standards, Innovation Academy for Precision Measurement Science and Technology, Chinese Academy of Sciences, Wuhan 430071, China
3Shanghai EBIT Laboratory, Key Laboratory of Nuclear Physics and Ion-Beam Application (MOE), Institute of Modern Physics, Fudan University, Shanghai 200433, China
4Institute of Applied Physics and Computational Mathematics, Beijing 100088, China
5Department of Physics, University of New Brunswick, Fredericton, New Brunswick, Canada E3B 5A3
6Department of Physics, University of Nevada, Reno, Nevada 89557, USA
7University of Chinese Academy of Sciences, Beijing 100049, China
8Max-Planck-Institut für Kernphysik, Heidelberg 69117, Germany

(Dated: January 27, 2021)

Highly charged ions (HCIs) are promising candidates for the next generation of atomic clocks, owing to their tightly bound electron cloud, which significantly suppresses the common environmental disturbances to the quantum oscillator. Here we propose and pursue an experimental strategy that, while focusing on various HCIs of a single atomic element, keeps the number of candidate clock transitions as large as possible. Following this strategy, we identify four adjacent charge states of nickel HCIs that offer as many as six optical transitions. Experimentally, we demonstrated the essential capability of producing these ions in the low-energy compact Shanghai-Wuhan Electron Beam Ion Trap. We measured the wavelengths of four magnetic-dipole (M1) and one electric-quadrupole (E2) clock transitions with an accuracy of several ppm with a novel calibration method; two of these lines were observed and characterized for the first time in controlled laboratory settings. Compared to the earlier determinations, our measurements improved wavelength accuracy by an order of magnitude. Such measurements are crucial for constraining the range of laser wavelengths for finding the “needle in a haystack” narrow lines. In addition, we calculated frequencies and quality factors, evaluated sensitivity of these six transitions to the hypothetical variation of the electromagnetic fine structure constant α needed for fundamental physics applications. We argue that all the six transitions in nickel HCIs offer intrinsic immunity to all common perturbations of quantum oscillators, and one of them has the projected fractional frequency uncertainty down to the remarkable level of 10−19.

I. INTRODUCTION

Quantum metrology of atomic time-keeping has seen dramatic improvements over the past decade with novel applications spanning from chronometric geodesy [1, 2] to fundamental physics, such as dark matter searches [3, 4] and multi-messenger astronomy [5]. Currently, optical atomic clocks using neutral atoms or singly charged ions have demonstrated fractional frequency uncertainties at the level of 10−18 or even 10−19 [6–9]. These uncertainties refer to the ability to protect the quantum oscillator from environmental perturbations, such as stray magnetic and electric fields. As these existing technologies mature, they are reaching the stage where one needs to understand numerous sources of environmental perturbations in greater detail. In some cases, the perturbations cannot be fully eliminated and one needs to devote significant efforts to measuring and characterizing the perturbations; these lead to non-universal systematic corrections to the clock frequency that are specific to experimental realization of the clock.

Novel classes of atomic clocks must start with quantum oscillators that offer a much more improved inherent immunity to environmental perturbations than the more mature technologies. One of such systems is the nuclear clock based on the unique property of the 229Th nucleus – the existence of a nuclear transition in a laser-accessible range [10, 11]; unfortunately, despite substantial worldwide efforts [12, 13], this transition is yet to be observed directly. The suppression of environmental perturbations for the nuclear oscillator comes from the nuclear size being ~ 104 times smaller than the size of a neutral atom. Alternative novel systems are highly charged ions (HCIs) [14, 15]. Similar to the nuclear clock, here the oscillator size is also substantially reduced, owing to the electronic cloud size shrinking as 1/Z with the increasing
ion charge $Z$. HCIs were proposed as promising candidates for the next generation of atomic clocks [14]. In addition, beyond the improved time-keeping, HCIs open intriguing opportunities for probing new physics beyond the standard model of particle physics [16, 17].

Compared to the single, yet to be spectroscopically found nuclear transition, there is a plethora of suitable HCIs (see a review [18] for a sample of proposals). A detailed analysis [19] indicates that with certain HCIs, atomic clocks “can have projected fractional accuracies beyond the $10^{-20} - 10^{-21}$ level for all common systematic effects, such as blackbody radiation, Zeeman, ac-Stark, and quadrupolar shifts”. Moreover, compared to the nuclear clock, where the direct observation of the clock transition remains elusive, the clock transitions in HCIs can be found with conventional spectroscopy or from atomic-structure computations. Indeed, here we report spectrographic measurements of wavelengths for five clock transitions with an accuracy of several ppm (see Table I), setting up the stage for the more accurate laser spectroscopy.

Despite the lack of suitable electric-dipole ($E1$) transitions for direct laser cooling, recent successes in sympathetic cooling and quantum logic spectroscopy of HCIs have paved way for precision spectroscopic measurements with HCIs [20, 21]. It is worth emphasizing that these newly demonstrated technologies can be applied universally to a wide range of HCIs. The multitude of suitable clock HCI candidates is a “blessing in disguise”, as one needs to commit to building the infrastructure for a specific ion. As with any new endeavor, one would like to mitigate potential problems with picking a “wrong” ion. Here we propose and pursue a straddling strategy that would allow one to explore several clock transitions using not only the same HCI production system but also ions of the same atomic element.

A suitable HCI has to possess a number of properties enabling precision spectroscopy and compatibility with operating an atomic clock. Generally, one may distinguish between three classes of visible or near visible optical forbidden transitions in HCIs that can be used for developing optical clocks:

1. Magnetic-dipole ($M1$) transitions between two hyperfine-structure levels of the same electronic state [19, 22].

2. Forbidden transitions between level crossing electronic states, which tend to be sensitive to variation of the fine structure constant [16, 23–25].

3. Forbidden transitions between the ground-state fine structure levels [14, 19, 26, 27].

Type 1 transitions occur in few-electron heavy HCIs [19] that are challenging to produce and trap. Type 2 transitions involve a complex energy structure that can impede initialization and read-out of the clock states. Here we focus on type 3 transitions that offer simplicity in both producing the ions and clock operation. More specifically we choose HCIs of nickel of various charge states [19, 26, 27]: Ni$^{11+}$, Ni$^{12+}$, Ni$^{14+}$, and Ni$^{15+}$. The clock transitions are shown in Fig. 1. All the traditional clock perturbations are strongly suppressed for these ions due to the charge scaling arguments [14, 19, 28]. As pointed out in Ref. [14], the major issue with HCI clocks is the so-called quadrupolar shift of the clock transition, when the quadrupole ($Q$) moment of the clock state couples to the always existing $E$-field gradients in ion traps. While the $Q$-moment of an electronic cloud does scale as $1/Z^2$, this reduction is not sufficient to suppress the quadrupolar shift below the desired level of accuracy. Thus, it is beneficial to select clock states with either vanishing or strongly suppressed $Q$-moments.

There are four $M1$ and two $E2$ optical transitions in Ni$^{11+}$, Ni$^{12+}$, Ni$^{14+}$, and Ni$^{15+}$ that offer the desired flexibility. These ions have varying number of electrons in the $3p$ shell, see Fig. 1. The clock transitions are between the fine structure components of the ground electronic state. There are four stable isotopes $^{58}$Ni, $^{60}$Ni, $^{62}$Ni, and $^{64}$Ni without nuclear spin; these can be used to search for new physics with isotope shift measurements [29–31] and for initial spectroscopic measurements. These spin-0 isotopes, however, will be susceptible to the quadrupolar shifts for clock transitions. However, these shifts can be suppressed by using the $^{61}$Ni isotope (nuclear spin $I = 3/2$), which has a natural abundance of 1.14%. Then the quadrupolar shifts can be either strongly suppressed or completely removed by employing the following clock transitions between hyperfine states (see Fig. 1):

- $^{2}P_{3/2}F = 0$ and $^{2}P_{1/2}F = 1$ or $F = 2$ for Ni$^{11+}$ and Ni$^{15+}$,
- $^{3}P_{1}F = 1/2$ and $^{3}P_{2}F = 1/2$ for Ni$^{12+}$,
- $^{3}P_{1}F = 1/2$ and $^{3}P_{0}F = 3/2$ for Ni$^{14+}$,
- $^{3}P_{0}F = 3/2$ and $^{3}P_{2}F = 1/2$ for Ni$^{12+}$ and Ni$^{14+}$.

This selection is based on the following reasoning [19]: $Q$-moments (rank 2 tensors) of the $F = 0$ and $F = 1/2$ states are zero due to selection rules. For the $^{2}P_{1/2}F = 1,2$ and $^{3}P_{0}F = 3/2$ states, the electronic $Q$-moments vanish due to selection rules for the electronic angular momentum $J$. Thereby, the $Q$-moments are determined by the nuclear $Q$-moments or hyperfine mixing [11] and, as such, are strongly suppressed. As an indication of attainable accuracy, Refs. [26, 27] evaluated relevant properties of the clock transitions in $^{61}$Ni$^{15+}$ and $^{58}$Ni$^{12+}$ and estimated common systematic uncertainties to be below $10^{-10}$, in line with the more general estimates of Ref. [19]. The second-order Doppler shift induced by the excess micromotion of the trapped ion is expected to be suppressed to below $10^{-19}$ by compensating the stray electric field to a level below 0.1 V/m [32, 33]. In a cryogenic trap, the heating rate of the trapped ions caused by the collisions with the background gas and the anomalous motional heating is reduced, and hence the second-order Doppler shift induced by the secular motion is also expected to
be sufficiently small [18]. Based on these arguments, we expect the attainable fractional systematic uncertainty of all the six clock transitions in Ni HCIs to be $10^{-19}$.

As the first essential step towards realizing the Ni HCI clocks, we produced the target ions at our newly built low-energy compact Shanghai-Wuhan Electron Beam Ion Trap (SW-EBIT) [34]. The wavelengths of four $M1$ and one $E2$ clock transitions between the ground-state fine structure levels in these ions are measured to an accuracy of several ppm using a spectograph. In particular, the three $M1$ lines $b$, $c$, and $g$ (listed in Table I) in Ni$^{12+}$ and Ni$^{14+}$ are observed and characterized for the first time in the laboratory. We also carried out calculations for these ions using an $ab$ initio relativistic method of atomic structure, the multi-configuration Dirac-Hartree-Fock (MCDHF) method [35, 36]. We evaluated relevant spectroscopic properties, such as transition wavelengths and natural linewidths. We also estimated the sensitivity to the hypothetical variation of the fine structure constant $\alpha$ and found that all considered clock transitions in Ni HCIs are more susceptible to the variation than most of the commonly employed singly charge ions or neutral atoms. Thus, Ni HCIs can be used for placing stringent constraints on the spatial or temporal variation of $\alpha$.

II. EXPERIMENTAL METHOD AND RESULTS

A. Production of Ni HCIs

To produce Ni HCIs, we injected the Ni(C$_5$H$_5$)$_2$ (nickelocene) molecular beam into the trap center. Then the charge-state distribution of Ni HCIs was measured using the electron-beam current of 6 mA and the electron-beam energy of 500 eV, which is higher than the ionization energies 319.5 eV, 351.6 eV, 429.3 eV, and 462.8 eV needed for Ni$^{11+}$, Ni$^{12+}$, Ni$^{14+}$, and Ni$^{15+}$, respectively. The extraction period was 0.3 s and the magnetic flux density was 0.16 T. As shown in Fig. 2, the target ions Ni$^{11+}$, Ni$^{12+}$, Ni$^{14+}$, and Ni$^{15+}$ were produced, and the ions of two distinct isotopes, $^{60}$Ni and $^{58}$Ni, were resolved. The techniques for measuring charge-state distribution are described in Ref. [34].

B. Spectral measurements

The spectra of the trapped Ni HCIs were observed by a Czerny-Turner spectograph (Andor Kymera 328i) equipped with an Electron Multiplying Charge-Coupled Device (EMCCD, Andor Newton 970, pixel: $1600 \times 200$, pixel size: $16 \mu m$) and a 1200 l/mm grating blazed at 500 nm. To maximize the number of the Ni HCIs of a specific charge state, different electron-beam energies were used, i.e. 370 eV, 400 eV, 500 eV, and 540 eV for Ni$^{11+}$, Ni$^{12+}$, Ni$^{14+}$, and Ni$^{15+}$, respectively. As illustrated in Fig. 3, the fluorescence emitted from the Ni HCIs was focused by a single N-BK7 Bi-Convex lens (focal length

---

**TABLE I.** Observed and calculated wavelengths of magnetic-dipole ($M1$) and electric-quadrupole ($E2$) transitions, where the lines $a$ through $f$ are candidate clock transitions, in nm.

| Line | Ion | Transition | Type | NIST Vacuum | Air (observed) Vacuum | This work Vacuum | Theory |
|------|-----|------------|------|-------------|-----------------------|------------------|--------|
| a    | Ni$^{11+}$ | 3$s^2$3$p^5$ P$_{1/2}$ - 3$s^2$3$p^5$ P$_{1/2}$ | M1   | 423.2       | 423.104(2)            | 423.223(2)       | 423.0(6) |
| b    | Ni$^{12+}$ | 3$s^2$3$p^4$ 3$P_1$ - 3$P_2$ | M1   | 511.724     | 511.570(2)            | 511.713(2)       | 511.8(6) |
| c    | Ni$^{14+}$ | 3$s^2$3$p^2$ 3$P_1$ - 3$P_0$ | M1   | 670.36      | 670.167(2)            | 670.352(2)       | 671.1(14) |
| d    | Ni$^{15+}$ | 3$s^2$3$p$ 3$P_2$ - 3$P_1$ | M1   | 360.22      | 360.105(2)            | 360.207(2)       | 359.9(9)  |
| e    | Ni$^{12+}$ | 3$s^2$3$p^4$ 3$P_0$ - 3$P_2$ | E2   | 498.50(249) |                       |                  | 496.9(24) |
| f    | Ni$^{14+}$ | 3$s^2$3$p^2$ 3$P_2$ - 3$P_0$ | E2   | 365.277     |                       |                  | 365.278(1) |
| g    | Ni$^{14+}$ | 3$s^2$3$p$ 2$P_2$ - 2$P_1$ | M1   | 802.63      | 802.419(2)            | 802.639(2)       | 800.3(25) |

---

**FIG. 1.** Partial energy-level diagrams for highly charged nickel ions. Clock transitions are explicitly drawn. Magnetic-dipole ($M1$) transitions are shown in magenta and electric-quadrupole ($E2$) transitions in green. The labeling of transitions is the same as in Table I.
f = 10 cm at 633 nm) on the spectrograph entrance slit. The distance between the trap (DT2, drift tube 2 in SW-EBIT [34]) center and the front principal plane of the lens remained fixed at 197 mm, which was about twice the focal length. Before setting up the spectrograph, a Charge-Coupled Device (CCD) was placed on the image plane to image the two inner edges of DT2 (1 mm slit width) that were illuminated by the hot cathode. In order to ensure that the lens was aligned with the optical axis, we adjusted the angle and position of the lens until the edge image became mirror-symmetric. Because of the dispersion of the lens, to ensure that the spectrograph slit was always precisely located on the image plane, the dispersion of the lens, to ensure that the spectrograph slit the edge image became mirror-symmetric. Because of the axis, we adjusted the angle and position of the lens until the edge image became mirror-symmetric. Because of the dispersion of the lens, to ensure that the spectrograph slit was always precisely located on the image plane, the distance L between the slit of the spectrograph and the back principal plane of the lens was calculated and adjusted for every central wavelength of the measured spectra. The grating was set to zero-order to image the inner edges of DT2 through spectrograph with its maximum slit width and minimum iris aperture behind the slit. Similarly, the angle and position of the spectrograph were adjusted until the image of the edges became mirror-symmetric to ensure the spectrograph alignment with the optical axis. A one inch aperture was placed before the lens to block the stray light. For calibration, a conjugated optical system was installed on the opposite side of the spectrograph. A diffuser attached by a 0.5 mm slit was placed on the object plane. A low-pressure gas-discharge lamp filled with Kr illuminated the slit, and the slit was imaged to the trap center to overlap with the trapped ion cloud. During the spectral exposure time of 10 to 60 minutes, the Kr lamp as the calibration light source flashed at a period of 1 to 3 minutes. The slit of the spectrograph was set to 30 μm, and the iris aperture in the spectrograph was set to 40 steps to obtain the F/7.6 aperture. The focal length of the spectrograph was tuned to minimize the linewidth in each spectral range.

All the spectra were binned to a non-dispersive direction after removing the cosmic ray noise, as shown in Fig. 4 (a). The dispersion function was obtained by fitting the NIST-tabulated Ritz in-the-air wavelengths of the calibration lines to a cubic polynomial, against their column numbers of the line centroids. The residuals of the calibration lines and the 1-σ fitting confidence band are shown in Fig. 4 (b). To determine the line centroids, the measured lines and calibration lines were fitted to a Gaussian or a multi-Gaussian profile, as shown in Fig. 4 (c).

### C. Observed wavelengths

Previously, these five M1 lines in Table I were observed in the solar corona emission [37] with a wavelength uncertainty of tens of picometer. The lines a and d have been also measured in Tokamak [38, 39], but experimental observation of the other three lines b, c, and g has not been reported in the literature. In this work, we observed and identified all five M1 lines emitted from the nickel plasma in the SW-EBIT in a controlled laboratory setting. The measured wavelengths agree with the Ritz wavelengths in NIST database [40], as shown in Table I, where the wavelengths between air and vacuum were converted by an empirical equation [41]. However, for line d, our result of 360.105(2) nm substantially deviates from the value of 360.123(2) nm observed from Tokamak plasma by Hinnoy et al. [39]. To test our result, two lines from Ar+(i.e., 358.843(2) nm, which are in good agreement with the Ritz wavelengths in NIST database, i.e., 357.661538 nm and 358.844021 nm. For the E2 lines e and f, the transition rates are too small to be observable by our technique. However, we deduced the wavelength of line f in Table I from those of lines c and g via the Rydberg-Ritz combination principle.

### D. Measurement uncertainties

#### Line centroid uncertainty

The line centroids of the measured lines and their calibration lines were determined by the centers of the fitted Gaussian profiles. Since the statistical uncertainty of the line centroid was mainly caused by the low signal-to-noise ratio, we evalu-
FIG. 4. (a) A spectrum of line $a$ from Ni$^{11+}$ and its calibration lines from Kr atom whose approximate wavelengths are labeled in the figure in nm. (b) Residuals of cubic polynomial fits of the calibration lines. The gray band is a 1-$\sigma$ confidence band. The uncertainties in the calibration lines are dominated by the line centroid uncertainties of the Gaussian fits. (c) Spectrum of line $a$ and its Gaussian fit.

ated the statistical uncertainty by performing at least 20 measurements on the line of interest, as shown in Fig 5. For all five measured lines, this uncertainty was smaller than 0.4 pm. The systematic uncertainty of the line centroid is mainly caused by the non-ideal Gaussianity of the line because of the optical aberration and the Zeeman components. In this work, since the measured lines and their calibration lines shared a similar profile, the optical aberration effect was largely offset. In the trap center, the magnetic flux density was $\sim 0.16$ T, resulting in a $\sim 2$ pm splitting between the Zeeman components of the clock transitions, which was relatively small (unresolved) compared to the $\sim 90$ pm linewidth. Furthermore, the Zeeman effect would not alter the line centroid because the Zeeman components were symmetrically distributed; in addition, the Zeeman effect was negligible for the Kr lamp due to the low magnetic field of 0.4 mT.

Dispersion function uncertainty. The statistical uncertainty for the dispersion function was caused by the centroid statistical uncertainties of calibration lines, which were reduced by the statistics of the line centroids. The systematic dispersion function uncertainty of a measured line was estimated by averaging the absolute values of the fitted residuals of its calibration lines of all the measured spectra.

Calibration systematic uncertainty. Since the image of the calibration light source might not be overlapped exactly with the trapped ion cloud, the spatial deviation and misalignment could cause wavelength offset between the measured lines and their calibration lines. In this work, a spatial deviation of less than 2 mm would result in a wavelength uncertainty of less than 1 pm. The misalignment could cause a wavelength uncertainty of less than 1 pm, which was estimated from five measurements of the Ar$^{3+}$ 553 nm line by resetting the optical system every time. Thereby, the overall systematic uncertainty caused by our calibration scheme was expected to be less than 2 pm.

Other uncertainties. In this work, the calibration light source and the fluorescence of the trapped ions were exposed to the spectrograph almost simultaneously, indicating that the temperature drift and the mechanical
drift were canceled out. The shifts due to the Stark effect and collisions can also be neglected at this level of accuracy. The wavelengths of the selected calibration lines are reliable because their uncertainties in the NIST database are all less than 0.3 pm.

Table II is the uncertainty budget for the lines \(a-d\) and \(g\) in air. The total uncertainty was calculated as the quadrature of all the uncertainties, which was dominated by the calibration systematic uncertainty. In order to test the reliability of the uncertainty estimation, the wavelengths in-the-air of uncertainty may be reduced by using a higher resolution spectrograph that is less sensitive to the calibration optical system.

### III. THEORETICAL METHOD AND RESULTS

#### A. MCDHF calculations

In the MCDHF method, an atomic wave function \(\Psi\) is constructed as a linear combination of configuration state functions (CSFs) \(\Phi\) of the same parity \(P\), the total angular momentum \(J\), and its projection \(M_J\), i.e.,

\[
\Psi(\Gamma P J M_J) = \sum_{i=1}^{N_{CSF}} c_i \Phi(\gamma_i P J M_J). \tag{1}
\]

Here \(c_i\) is the mixing coefficient and \(\gamma_i\) stands for the remaining quantum numbers of the CSFs. Each CSF itself is a linear combination of products of one-electron Dirac orbitals. Both mixing coefficients and orbitals are optimized in the self-consistent field calculation. After a set of orbitals is obtained, the relativistic configuration interaction (RCI) calculations are used to capture more electron correlations. In addition to the Coulomb interactions, our RCI calculations also include the Breit interaction in the low-frequency approximation and the quantum electrodynamic (QED) corrections.

In order to obtain high-quality atomic wave functions, we designed an elaborate computational model as follows. In the first step, the self-consistent field (SCF) calculations were performed successively to generate virtual orbitals. The virtual orbitals were employed to form CSFs which account for certain electron correlations. More specifically, CSFs were produced through single (S)- and double (D)-electron excitations from the occupied Dirac-Hartree-Fock orbitals to virtual orbitals, but the double excitation from the atomic core \(1s^22s^22p^6\) orbitals were excluded at this stage. The virtual orbitals were augmented layer by layer up to \(n_{\text{max}} = 12\) and \(l_{\text{max}} = 6\), where \(n_{\text{max}}\) and \(l_{\text{max}}\) denote, respectively, the maximum principal quantum number and the maximum angular quantum number of the virtual orbitals. In the second step, the single-reference configuration RCI calculations were performed with the configuration space constructed from SD excitation from all occupied orbitals to the set of virtual orbitals. In other words, the correlation between electrons in the atomic core, which were neglected in the first step, were captured. In the last step, we considered part of contributions from the triple- and quadruple-excitation CSFs. In order to limit the number of CSFs, the MR-SD approach was adopted to produce corresponding CSFs [46, 47]. The multi-reference (MR) configuration sets were created as \(\{3s3p^33d, 3s^23p^33d^2\}\) for \(\text{Ni}^{11+}\), \(\{3s3p^33d, 3s^23p^23d^2, 3p^6\}\) for \(\text{Ni}^{12+}\), \(\{3s3p^23d, 3s^23d^2, 3p^4\}\) for \(\text{Ni}^{14+}\), and \(\{3p^3, 3s3p3d, 3p3d^2\}\) for \(\text{Ni}^{15+}\). Additionally, the Breit interaction and the QED corrections were included in the RCI computation.

Once the atomic wave functions are obtained, we are in a position to calculate the physical quantities under investigation, that is, the reduced matrix elements for corresponding rank \(k\) irreducible tensor operators between two atomic states, i.e., \(\langle \Psi(\Gamma P J) | O^{(k)} | \Psi(\Gamma' P' J') \rangle\). The magnetic dipole and electric quadrupole transition operators are rank 1 and rank 2 operators, respectively. In practice, we performed the calculations using the GRASP2018 package [48].

#### B. Calculated wavelengths

As shown in Table I, the calculated wavelengths of the \(M1\) transitions of line \(a\) through line \(d\) and line \(g\) agree with our measured values. The wavelengths of the two \(E2\) transitions of line \(e\) and line \(f\) in \(\text{Ni}^{12+}\) and \(\text{Ni}^{14+}\) were also calculated. These two lines have not been observed yet before. Our calculated wavelengths for these two transitions are in agreement with the NIST recommended values. Meanwhile, the calculated wavelength of line \(f\) also agrees with our indirect measurement, see
Table I.

C. Properties of the clock transitions

The design of an atomic clock relies on the knowledge of atomic parameters of the quantum oscillator. Thus, we have computed wavelengths, spontaneous emission rates $A$, lifetimes $\tau$, linewidths $\Gamma$ (2$\Gamma$ = 1/$\tau$), and other parameters for all six candidate clock transitions, and the results are listed in Table III. As one of the key parameters of clock stability, the quality factor (Q-factor) is also given in this table. The Q-factor is defined as the ratio of the clock frequency $\nu_{\text{clk}}$ to the linewidth $\Gamma$ of the clock transition, i.e., $Q = \nu_{\text{clk}}/\Gamma$. Among the four $M1$ clock transitions, the $3P_1 - 3P_0$ transition in Ni$^{14+}$ is the narrowest with its linewidth less than 10 Hz, while the linewidths of the other three $M1$ transitions are about 30 Hz. The corresponding Q-factors of these four $M1$ transitions are $\sim 10^{13}$. There are two decay channels from $3P_0$ in Ni$^{12+}$ and $3P_2$ in Ni$^{14+}$ to the lower states. In order to determine the linewidth of these $E2$-clock transitions, both decay channels should be taken into account. For $3P_0$ in Ni$^{12+}$, the decay rate is 0.037 s$^{-1}$ for the $E2$ ($3P_0 - 3P_2$) channel and 0.011 s$^{-1}$ for the $M1$ ($3P_0 - 3P_1$) channel. For $3P_2$ of Ni$^{14+}$, the $E2$ ($3P_2 - 3P_0$) and $M1$ ($3P_2 - 3P_1$) transition rates are 0.03 s$^{-1}$ and 22.5 s$^{-1}$, respectively. Therefore, the linewidths for the $E2$-clock transitions are 3.6 Hz for $3P_2 - 3P_0$ in Ni$^{14+}$ and 8 mHz for $3P_0 - 3P_2$ in Ni$^{12+}$, which are respectively smaller than the $M1$ transition lines $c$ and $b$, as marked in Fig. 1. This $E2$ transition in Ni$^{12+}$ is particularly attractive for stable clockwork [27], because of its relatively high Q-factor of $7.5 \times 10^{16}$, meaning that the statistical uncertainty limited by the quantum projection noise [18, 49, 50] of this transition can reach the level of $10^{-19}$ by averaging over a few days.

From the perspective of searching for new physics, we anticipate that by monitoring the Ni HCl clock transition frequencies, stringent constraints could be placed on the possible time variation of the fine structure constant $\alpha$. Following Refs. [17, 52], one can introduce the “sensitivity coefficient” $q_x$, defined by $\omega(x) = \omega_0 + q_x$, where $x \equiv (\alpha/\alpha_0)^2 - 1$ and $\omega_0$ is the clock transition frequency at the nominal value of the fine structure constant $\alpha_0$. The sensitivity coefficient $q_x$ characterizes the linear response of the clock frequency $\omega(x)$ to the variation of $\alpha$, and can be calculated numerically as $q_x \approx [\omega(+) - \omega(-)]/(2x)$. Another commonly used quantity is the dimensionless enhancement factor [17] $K = \partial \ln \omega/\partial \ln \alpha$ $\approx 2q_0/\omega_0$. As shown in Table III, our computed $K$ values for the relevant transitions in nickel HClIs are about 2, which is higher than most of the current optical clocks. For example [53], Al$^+$ has $K = 0.008$. Out of $\sim 10$ species currently used in the optical clock community, only the heavy Yb$^+$ and Hg$^+$ ions have $|K| > 2$ [53]. Therefore, we expect that, even with their initial predicted accuracy of $10^{-19}$, the quantum clocks based on the relatively light Ni HClIs will have greater potential for exploring new physics than most of the current atomic clocks. Recently, an improved constraint of $\delta/\alpha = 1.0(1.1) \times 10^{-18}$ year was reported based on the comparison of the $^2S_{1/2}(F = 0) - ^2D_{3/2}(F = 2)$ (E2, $K = 1.00$) and the $^2S_{1/2}(F = 0) - ^2F_{7/2}(F = 3)$ (E3, $K = -5.95$) transition of $^{171}$Yb$^+$ clock [54]. The constraint on the temporal variation of $\alpha$ is expected to be further improved by comparing two clocks based on the $E2$ transition of Ni$^{12+}$ and the E3 transition of Yb$^+$, because of its larger $K$ value and smaller projected systematic and statistical uncertainties of the $E2$ transition in Ni$^{12+}$ than those of the $E2$ transition in Yb$^+$.

Nandy and Sahoo [51] determined the sensitivity coefficient to the $\alpha$-variation for the $2P_{1/2} - 2P_{3/2}$ transition in Ni$^{11+}$ ion. In their work, the transition rate and the lifetime of the $2P_{1/2}$ state were calculated using the relativistic coupled-cluster (RCC) method. Yu and Sahoo [26, 27] calculated some atomic parameters for the $2P_{3/2} - 2P_{1/2}$ transition in Ni$^{15+}$ and the $2P_0 - 2P_2$ transition in Ni$^{12+}$ with the RCC and MCDHFs methods. Their results are also listed in Table III for comparison. For lines $a$, $d$, and $e$, our calculated values agree well with other theoretical results [26, 27, 51], except for a factor of 3 difference for the sensitivity coefficient $q$ of line $d$. There is also a factor of 6 difference in the value of the $Q$-factor of line $e$, for which we traced back to the trivial factor of $2\pi$ missing in the linewidth definition in Ref. [27].

Previous theoretical work on nickel HClIs focuses on atomic properties relevant to the emission from the solar, astrophysical, and laboratory plasmas. In Tables IV and V, we present a comparison with the literature values for the spontaneous decay rates and lifetimes. Overall, our MCDHF values agree well with the results from other theoretical methods, such as the RCC method and the multi-reference Møller-Plesset perturbation theory. Moreover, the lifetimes of the $2P_{1/2}$ state in Ni$^{11+}$ ion, the $3P_1$ state in Ni$^{12+}$ ion, and the $2P_{3/2}$ state in Ni$^{15+}$ ion were measured at the heavy-ion storage ring [55–57]. We found a good agreement between theory and experiment.

D. Computational uncertainties

The computational uncertainties in our work include the neglected correlation contributions, such as the triple- and quadruple-electron excitations involving the $1s$ orbital. The upper limit on these effects was estimated from the double excitations of the core orbitals in the single-reference configuration RCI calculations. The “truncation” uncertainties due to the finite number of virtual orbitals were evaluated based on the convergence trends in the above-mentioned three steps. For the wavelengths, all the uncertainties were summed together in quadrature. For the $M1$ transition rates, in addition to these uncertainties, we also included the
frequency-dependent Breit interaction contribution as another source of error. For the E2 transition rates, the difference in results between the Babushkin and Coulomb gauges [75] were treated as an additional contribution to the combined theoretical uncertainty.

### IV. CONCLUSIONS

To reiterate, the quantum clockwork we explored here provides an intriguing possibility for achieving high accuracy on multiple transitions in HClIs of the same element. Our strategy offers an important flexibility in the pursuit of multiple candidate clock transitions. Particularly, the E2 transition in $^{63}$Ni$^{12+}$ has projected fractional uncertainty $10^{-19}$. We demonstrated the key experimental capabilities of using our SW-EBIT facility to generate and extract Ni$^{11+}$, Ni$^{12+}$, Ni$^{14+}$, and Ni$^{15+}$ ions. We measured the wavelengths of four M1 and one E2 clock transitions in these ions with the uncertainties of about 2 pm. The measured wavelengths establish an important reference for precision laser spectroscopy in future clock transition measurements. We also calculated spectroscopic properties of the relevant M1 and E2 clock transitions. The calculated wavelengths are consistent with our experimental results and with previous determinations. The calculated properties indicate that these ions are suitable for precision quantum metrology and for exploring new physics beyond the standard model of particle physics.

### ACKNOWLEDGMENTS

The authors thank Xin Tong, José R. Crespo López-Urrutia, and Yan-Mei Yu for helps and for fruitful discussions. This work was supported by the Strategic Priority Research Program of the Chinese Academy of Sciences (Grant No. XDB21030300), the National Natural Science Foundation of China (Grant Nos. 11934014, 11622434, 11974382, 11604369, 11974080, 11704398, and 11874090), the National Key Research and Development Program of China under Grant No. 2017YFA0304402, the CAS Youth Innovation Promotion Association (Grant Nos. Y201963 and 2018364), the Hubei Province Science Fund for Distinguished Young
Table V. Lifetimes (in ms) of upper clock states in Ni$^{11+}$, Ni$^{12+}$, Ni$^{14+}$, and Ni$^{15+}$. Numbers in square brackets stand for the powers of 10, i.e., $x \times 10^y$.

| Ion State | This work | Other theory | Experiment |
|-----------|-----------|--------------|------------|
| Ni$^{11+}$ - $P_{1/2}$ | 4.2(1) | 4.25 [58], 4.23(2) [51] | 4.166(60) [55] |
| Ni$^{12+}$ - $P_3$ | 6.3(1) | 6.5 [27], 6.55 [73], 6.59 [73] | 7.3(2)*, 6.50(15)** [56] |
| Ni$^{12+}$ - $P_{21/2}$ | 21.3(3) | 22.13 [73], 19.53 [73], 19.3 [27] |
| Ni$^{14+}$ - $P_3$ | 17.8(2) | 17.8 [67], 17.7 [70] |
| Ni$^{14+}$ - $P_2$ | 44(1) | 44.6 [67], 45.1 [70] |
| Ni$^{15+}$ - $P_{3/2}$ | 5.2(1) | 5.2 [72], 5 [26], 5.184 [74] | 5.90(1)*, 5.27(7)** [57] |

**Single exponential evaluation**

**Multi-exponential evaluation**

Scholars (Grant No. 2017CFA040), and the K. C. Wong Education Foundation (Grant No. GJTD-2019-15). ZCY was supported by NSERC of Canada. Work of A.D. was supported in part by the U.S. National Science Foundation.

[1] C. W. Chou, D. B. Hume, T. Rosenband, and D. J. Wineland, Science 329, 1630 (2010).
[2] R. Bondarescu, M. Bondarescu, G. Hetényi, L. Boschi, P. Jetzer, and J. Balakrishna, Geophys. J. Int. 191, 78 (2012).
[3] A. Derevianko and M. Pospelov, Nat. Phys. 10, 933 (2014).
[4] A. Arvanitaki, J. Huang, and K. Van Tilburg, Phys. Rev. D 91, 015015 (2015).
[5] C. Dailey, C. Bradley, D. F. J. Kimball, I. Sultai, S. Pustelny, A. Wickenbrock, and A. Derevianko, arXiv:2002.04352 (2020).
[6] S. M. Brewer, J. S. Chen, A. M. Hankin, E. R. Clements, C. W. Chou, D. J. Wineland, D. B. Hume, and D. R. Leibrandt, Phys. Rev. Lett. 123, 33201 (2019).
[7] N. Huntemann, C. Sanner, B. Lipphardt, C. Tamm, and E. Peik, Phys. Rev. Lett. 116, 063001 (2016).
[8] W. F. McGrew, X. Zhang, R. J. Fasano, S. A. Schäffer, K. Beloy, D. Nicolodi, R. C. Brown, N. Hinkel, G. Milani, M. Schioppo, T. H. Yoon, and A. D. Ludlow, Nature 564, 87 (2018).
[9] E. Oelker, R. B. Hutson, C. J. Kennedy, L. Sonderhouse, T. Bothwell, A. Gohar, D. Kedar, C. Sanner, J. M. Robinson, G. E. Marti, D. G. Matei, T. Legero, M. Giunta, R. Holzwarth, F. Riehle, U. Stern, and J. Ye, Nat. Photonics 13, 714 (2019).
[10] E. Peik and C. Tamm, Europhysics Letters (EPL) 61, 181 (2003).
[11] C. J. Campbell, A. G. Radnaev, A. Kuzmich, V. A. Dzuba, V. V. Flambaum, and A. Derevianko, Phys. Rev. Lett. 108, 120802 (2012).
[12] L. Von Der Wense, B. Seiferle, M. Laatiaoui, J. B. Neu-mayr, H. J. Maier, H. F. Wirth, C. Mokry, J. Runke, K. Eberhardt, C. E. Düllmann, N. G. Trautmann, and P. G. Thirolf, Nature 533, 47 (2016).
[13] B. Seiferle, L. von der Wense, P. V. Bilous, I. Amersdorffer, C. Lemell, F. Libisch, S. Stellmer, T. Schumm, C. E. Düllmann, A. Païffy, and P. G. Thirolf, Nature 573, 243 (2019).
[14] A. Derevianko, V. A. Dzuba, and V. V. Flambaum, Phys. Rev. Lett. 109, 180801 (2012).
[15] M. S. Safronova, V. A. Dzuba, V. V. Flambaum, U. I. Safronova, S. G. Porsev, and M. G. Kozlov, Phys. Rev. Lett. 113, 030801 (2014).
[16] J. C. Berengut, V. A. Dzuba, and V. V. Flambaum, Phys. Rev. Lett. 105, 120801 (2010).
[17] M. S. Safronova, D. Budker, D. Demille, D. F. Kimball, A. Derevianko, and C. W. Clark, Rev. Mod. Phys. 90, 25008 (2018).
[18] M. G. Kozlov, M. S. Safronova, J. R. Crespo López-Urrutia, P. O. Schmidt, J. R. C. López-Urrutia, and P. O. Schmidt, Rev. Mod. Phys. 90, 045005 (2018).
[19] V. I. Yudin, A. V. Taichenachev, and A. Derevianko, Phys. Rev. Lett. 113, 233003 (2014).
[20] P. Mieke, T. Leopold, S. A. King, E. Benkler, L. J. Spieß, L. Schmöger, M. Schwarz, J. R. Crespo López-Urrutia, and P. O. Schmidt, Nature 578, 60 (2020).
[21] L. Schmoger, O. O. Versolato, M. Schwarz, M. Kohnen, A. Windberger, B. Piest, S. Feuchtenbeiner, J. Pedregosa-Gutierrez, T. Leopold, P. Mieke, A. K. Hansen, T. M. Baumann, M. Drewsen, J. Ullrich, P. O. Schmidt, and J. R. Crespo López-Urrutia, Science 347, 1233 (2015).
[22] S. Schiller, Phys. Rev. Lett. 98, 180801 (2007).
[23] J. C. Berengut, V. A. Dzuba, V. V. Flambaum, and A. Ong, Phys. Rev. Lett. 106, 210802 (2011).
[24] H. Bekker, A. Borschevsky, Z. Harman, C. H. Keitel, J. Pedregosa-Gutierrez, T. Leopold, P. Mieke, A. K. Hansen, T. M. Baumann, M. Drewsen, J. Ullrich, P. O. Schmidt, and J. R. Crespo López-Urrutia, Nature 578, 60 (2020).
[25] V. A. Dzuba, A. Derevianko, and V. V. Flambaum, Phys. Rev. A 86, 054501 (2012).
[26] Y. M. Yu and B. K. Sahoo, Phys. Rev. A 94, 062502 (2016).
[27] Y. M. Yu and B. K. Sahoo, Phys. Rev. A 97, 014103(R) (2018).
[28] J. C. Berengut, V. A. Dzuba, V. V. Flambaum, and A. Ong, Phys. Rev. A 86, 022517 (2012).
[29] I. Counts, J. Hur, D. P. L. Aude Craik, H. Jeon, C. Leung, J. C. Berengut, A. Geddes, A. Kawasaki, W. Jhe, and V. Vuletić, Phys. Rev. Lett. 125, 123002 (2020).
[30] C. Solaro, S. Meyer, K. Fisher, J. C. Berengut, E. Fuchs, and M. Drewsen, Phys. Rev. Lett. 125, 123003 (2020).
