Maximum likelihood estimation-assisted ASVSF through state covariance-based 2D SLAM algorithm

Heru Suwoyo¹, Yingzhong Tian², Wenbin Wang³, Long Li¹, Andi Adriansyah⁵, Fengfeng Xi⁶, Guangjie Yuan⁷

¹,²,⁴,⁷ School of Mechatronic Engineering and Automation, Shanghai University, Shanghai, China
²,⁴,⁷ Shanghai Key Laboratory of Intelligent Manufacturing and Robotics, Shanghai, China
¹,⁵ Department of Electrical Engineering, Universitas Mercu Buana, Jakarta, Indonesia
³ Mechanical and Electrical Engineering School, Shenzhen Polytechnic, Guangdong, China
⁶ Department of Mechanical, Aerospace, and Industrial Engineering, Ryerson University, Toronto, Canada

ABSTRACT

The smooth variable structure filter (ASVSF) has been relatively considered as a new robust predictor-corrector method for estimating the state. In order to effectively utilize it, an SVSF requires the accurate system model, and exact prior knowledge includes both the process and measurement noise statistic. Unfortunately, the system model is always inaccurate because of some considerations avoided at the beginning. Moreover, the small addictive noises are partially known or even unknown. Of course, this limitation can degrade the performance of SVSF or also lead to divergence condition. For this reason, it is proposed through this paper an adaptive smooth variable structure filter (ASVSF) by conditioning the probability density function of a measurement to the unknown parameters at one iteration. This proposed method is assumed to accomplish the localization and direct point-based observation task of a wheeled mobile robot, TurtleBot2. Finally, by realistically simulating it and comparing to a conventional method, the proposed method has been showing a better accuracy and stability in term of root mean square error (RMSE) of the estimated map coordinate (EMC) and estimated path coordinate (EPC).

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Corresponding Author:
Heru Suwoyo
School of Mechatronic Engineering and Automation
Shanghai University
Shanghai, 200444 China
Email: heru.suwoyo@mercubuana.ac.id

1. INTRODUCTION

The presence of a map can be useful for a mobile robot to perform its navigation task. Unfortunately, the consistent map is unavailable at the beginning [1]. Consequently, the system should be able to track the robot path and to build a map based on the robot measurement [2-4]. It can be done by knowing the current pose when sensing a feature and locating the pose based on the around features [5]. Since these tasks should be addressed at the same time, the definition of simultaneous localization and mapping (SLAM) is stated [6-12]. The SLAM-based mobile robot navigation has intensively received attention because of some challenging factors that need to be solved such as wide uncertainty, system complexity, inaccurate system model, limited...
prior information, noise statistics of the process and measurement, computational cost and filter divergence [13, 14].

Additionally, in the mobile robot application, the successful of solving SLAM problem can be validated root mean square error (RMSE) [15-17] calculated based on the different of the estimated and true value. The continuously grown uncertainty makes the estimated values deviates from its base. For this reason, the probability-based filtering method has been intensively used. It has been frequently adopted to effectively represent all the possibility related to the system [18]. The most popular one is extended kalman filter which has the basic task to update the state and covariance with an assumption all the related variable comply with Gaussian distribution. Generally, extended kalman filter [11, 19-23] is known as an nonlinear version of its predecessor named kalman filter [18-20, 24-28]. The easiness to apply extended kalman filter makes it has been widely used to solve in many different fields such as for the state and parameter estimation including SLAM, signal processing, fault detection and diagnosis and target tracking [29]. Nevertheless, it has many incompatibilities and difficulties such as the deviant solution from the state trajectory, less optimal state estimation and large estimation error due to the linearization process and computational cost [14, 15, 17]. These limitations make its practical application becomes limited nowadays.

Furthermore, many researcher have switched to use the similar method that might offered better robustness rather than EKF such as unscented kalman filter (UKF) [20, 30-32], cubature kalman filter (CKF) [15, 16, 26] smooth variable structure filter (SVSF) [15-17, 33], etc. Their recorded successes have been proving to have significant improvement of EKF. Among of them, SVSF has been rapidly developed. The SVSF is a relative new predictor-estimator, which is first invented in 2007 [15, 16]. Firstly, it was derived from a variable structure filter (VSF)[34] and extended variable structure filter (EVSF) [13, 17, 35]. Then proceed with a presence of new form by completing it with the error covariance matrix without affecting its accuracy and stability [35, 36]. As a common filtering technique, it was then enhanced by involving the time-varying boundary layer width to replace its previous characteristic [36, 37]. Due to these developments, SVSF becomes the popular method to against the uncertainty which is not only suitable for the linear but also nonlinear system [15-17]. Additionally, based on its characteristic, the SVSF can be combined with different methods in obtaining the optimal solution [15-17, 33, 34]. However, like the other traditional filter methods, to apply SVSF the noise statistic is often predefined to be fixed and constant for the whole estimation process. It often leads to divergence and degradation performance. Thus, traditional SVSF should at least be enhanced to partially estimating the noise statistic. Therefore, through this paper, SVSF is adaptively improved. Firstly, the SVSF’s error covariance matrix is mathematically derived via maximum a likelihood estimator [38]. It aims to recursively update the process covariance matrix $Q$ as well as the measurement error covariance matrix $R$. Since the prediction step of SVSF [15, 16, 33, 34] is totally same as EKF, so that, the innovation error can be similarly computed. Consequently, the derivation process of finding the compact formulation of $Q$ and $R$ is easy to be evaluable [31, 38]. Additionally, since this algorithm is used to solve SLAM problem, henceforth it is termed as ASVSF-SLAM algorithm in this paper. In case of knowing the performance of this algorithm, the proposed algorithm is realistic simulated and compared with traditional SLAM algorithm. Based on the comparative results, it can be declared that the ASVSF-SLAM algorithm can significantly solve the SLAM problem of wheeled mobile robot in term of RMSE for both estimated path coordinate and estimated map coordinate.

The rest parts of this paper are arranged as follows. Section 2 presents a discussion of the original SVSF. Section 3 sequentially presents the mathematical derivation conducted to find the recursive error covariance matrix of both the process and measurement noise statistic. Section 4 discuss an algorithm named ASVSF-SLAM algorithm with expansion of kinematic configuration and motion model, direct point-based observation and, inverse point-based observation. Finally, Section 5 presents a conclusion according to the result discussed in previous section.

2. CLASSICAL SVSF

Considering that the dynamic model of Gaussian nonlinear system is given as follows

\[
\begin{align*}
    x_k &= f(x_{k-1}, u_k) + \omega_{k-1} \\
    z_k &= h(x_k) + \nu_k
\end{align*}
\]

where $k$ is discrete time index, $x \in \mathbb{R}^n$ is the state vector, $u$ is the control vector and $z \in \mathbb{R}^m$ is the measurement...
vector. While, \( \omega \in R^n \) and \( \nu \in R^m \) are small process, and measurement noise, respectively. Whereas, \( f(\cdot) \) and \( h(\cdot) \) are the nonlinear function and measurement model, respectively. The statistical characteristic of this dynamic model is given as follows

\[
\begin{align*}
E[\omega_k] &= 0, \text{Cov}[\omega_k, \omega_j] = Q_k \delta_{kj} \\
E[\nu_k] &= 0, \text{Cov}[\nu_k, \nu_j] = R_k \delta_{kj} \\
E[\omega_k, \nu_j] &= 0
\end{align*}
\]

where \( \delta \) is Kronecker delta function. Meanwhile, \( E[\cdot] \) and \( \text{Cov}[\cdot, \cdot] \) are mean and covariance term, respectively. Then the complete formulation of SVSF can be chained as follows

\[
\hat{x}_{k|k-1} = f(\hat{x}_{k-1|k-1}, u_k) + q_{k-1}
\]

\[
P_{k|k-1} = FP_{k-1|k-1}F^T + Q_k
\]

\[
e_{z,k|k-1} = z_k - h(\hat{x}_{k|k-1}) - r_k
\]

\[
A = |e_{z,k|k-1}|_{abs} + \gamma |e_{z,k-1|k-1}|_{abs}
\]

\[
\psi = (A^{-1}HP_{k|k-1}H^T(HP_{k|k-1}H^T + R_k)^{-1})^{-1}
\]

\[
\text{sat}[\psi^{-1}e_{z,k|k-1}] = \left\{ \begin{array}{l}
1, \quad \psi^{-1}e_{z,k|k-1} \geq 1 \\
\psi^{-1}e_{z,k|k-1}, \quad -1 \leq \psi^{-1}e_{z,k|k-1} \leq 1 \\
-1, \quad \psi^{-1}e_{z,k|k-1} \leq -1
\end{array} \right.
\]

\[
K_k^{SVSF} = H^+ \{ A \circ \text{sat}[\psi^{-1}e_{z,k|k-1}] \} [e_{z,k|k-1}]^{-1}
\]

\[
\hat{x}_{k|k} = \hat{x}_{k|k-1} + K_k^{SVSF}e_{z,k|k-1}
\]

\[
P_{k|k-1} = (I - H K_k^{SVSF})e_{z,k|k-1}e_{z,k|k-1}^T(I - H K_k^{SVSF})^T + K_k^{SVSF} R_k K_k^{SVSF^T}
\]

\[
e_{z,k|k} = z_k - h(\hat{x}_{k|k}) - r_k
\]

\[
|e_{z,k-1|k-1}|_{abs} > |e_{z,k|k-1}|_{abs}
\]

3. **ESTIMATING THE NOISE STATISTIC**

Traditionally, SVSF has no ability to approximate the responsive noise statistic. Consequently, the possibility of divergence still high in case of either the realistic simulation or real application. Moreover, inaccurate modelled system might also increase the uncertainty that is precisely lead to degradation of filter performance. For this reason, an effort to complete SVSF with recursive noise statistic is proposed in this paper. This process can be done by estimating error matrix of the noise statistic by deriving the predicted error covariance matrix of the state using MLE [31, 38].

First, by recalling the innovation sequence of SVSF and considering that the nonlinear system (1) is Gaussian. According to [38, 39] and [6], \( S_k \) can also be alternatively calculated as

\[
\hat{C}_k = \sum_{j=k-N+1}^{k} d_j f_j^T
\]
where \( d_k \) is innovation sequence error as shown in (5), \( \hat{C}_k \) is alternative form of \( S_k \), and the addition of \( \sum_{j=k-N+1}^{k} d_j d_j^T \) is the moving window [40] for \( N \) refers to the window size.

Now, by recalling as shown in (2) and assuming that the unknown parameter \( \alpha = \{Q, R\} \), the adaptation process is done with assumptions that State vector \( x \) is not depend on \( \alpha \) i.e \( \frac{\partial x}{\partial \alpha} \), \( F \) and \( H \) are independent of \( \alpha \) and time variant, \( \epsilon_k \) is white and ergodic sequence within the estimation window, and \( S_k \) is regarded as the main key of adaption on depend parameters. Therefore, the probability density function of the measurements conditioned on the parameter \( \alpha \) at time \( k \) can be described as follows [31, 38]

\[
P(z|\alpha)_k = \left(\frac{2\pi}{|C_k|}\right)^{\frac{n}{2}} \exp \left( -\frac{1}{2} \| d_k \|_{C_k^{-1}}^2 \right) \tag{15}\]

Then by taking its algorithm, and ignoring all the constants, the compact formulation of shown in (15) is

\[
J(\alpha) = \sum_{j=k-N+1}^{k} d_j^T C_j^{-1} d_j = \min \tag{16}\]

Next, by adopting two relations of matrix differential calculus [38], (16) is derived as follows

\[
J(\alpha) = \sum_{j=k-N+1}^{k} \left[ \text{tr}\left\{ C_j^{-1} \frac{\partial C_j}{\partial \alpha} \right\} - d_j^T C_j^{-1} \frac{\partial C_j}{\partial \alpha} C_j^{-1} d_j \right] = \min \tag{17}\]

At this point, it is clear that the adaptive SVSF lies on the determination of \( C \) and its partial derivative with respect to \( \alpha \). Additionally, the main interest is in \( R_k \) and \( Q_k \) instead of \( C \) [31, 41, 42]. Therefore, by sequentially referring to (6), first derivative of \( C \) with respect to \( \alpha \), and a condition of \( P_{k-1|k-1} \) in the steady state, (17) can be compactly expressed as follows

\[
\sum_{j=k-N+1}^{k} \text{tr}\left\{ [C_j^{-1} - C_j^{-1} d_j d_j^T C_j^{-1}] [H \frac{\partial Q_j}{\partial \alpha} H^T + \frac{\partial R_j}{\partial \alpha}] \right\} = 0 \tag{18}\]

At this point, the process of obtaining both the adaptive estimation of the process noise and measurement noise covariance are presented. First, \( Q \) is assumed to be known and independent of \( \alpha \) to obtain the explicit expression for \( R \). Similarly, the process to gain the expression for \( Q \) will also involve the assumption that \( R \) is fixed and independent of \( \alpha \) at the previous process. Both processes can be sequentially described at the following subsection

3.1. Adaptive covariance matrix of process noise statistic

Given \( R \) then (18) becomes

\[
\sum_{j=k-N+1}^{k} \text{tr}\left\{ HC_j^{-1} H^T - HC_j^{-1} d_j d_j^T C_j^{-1} H^T \right\} = 0 \tag{19}\]

Then by referring to (7) after replacing \( S_k \) by \( C_k \), the alternative formulation of \( C_k^{-1} \) is obtained as follows

\[
C_k^{-1} H^T = \psi^{-1} AH^+ P_{k|k-1}^{-1} \tag{20}\]

Since, \( \psi^{-1} AH^+ \) is gain of SVSF on (9), and the saturation function on (8) is satisfied at the previous step, then it is clear to have the following form

\[
C_k^{-1} H^T = K_k^{SVSF} P_{k|k-1}^{-1} \tag{21}\]

Since (21) is formed then by substituting (21) into (19), it yields
respectively. Then by substituting (4) into (25), it yields
\[ \sum_{j=k-N+1}^{k} \text{tr}\left\{ P_j^{-1} K_j^{SVSF} H P_j - K_j^{SVSF} d_j d_j^T K_j^{SVSF^T} \right\} P_j^{-1} = 0 \] (22)

where \( P_j \) is \( P_{k|k-1} \). By definition, it should be at least semi-definite positive matrix, thus \( P_j^{-1} \) can be vanished.

As well-known that the alternative formulation of (11) is
\[ P_{k|k} - P_{k|k-1} = K_k^{SVSF} H P_{k|k-1} \] (24)

Now, substituting (10) and (24) into (23), it yields
\[ \sum_{j=k-N+1}^{k} \text{tr}\left\{ P_j^+ - P_j^- - [(\hat{x}_j^+ - \hat{x}_j^-)(\hat{x}_j^+ - \hat{x}_j^-)^T] \right\} = 0 \] (25)

Note that \( P^+ \) and \( P^- \) refer to \( P_{k|k} \) and \( P_{k|k-1} \), respectively. Meanwhile, \( \hat{x}^+ \) and \( \hat{x}^- \) refer to \( \hat{x}_{k|k} \) and \( \hat{x}_{k|k-1} \), respectively. Then by substituting (4) into (25), it yields
\[ \sum_{j=k-N+1}^{k} P_j^+ - FP_j^+ F^T - Q - [(\hat{x}_j^+ - \hat{x}_j^-)(\hat{x}_j^+ - \hat{x}_j^-)^T] = 0 \] (26)

Finally, the covariance matrix of process noise statistic is obtained
\[ \hat{Q} = \sum_{j=k-N+1}^{k} P_j^+ - FP_j^+ F^T - (\hat{x}_j^+ - \hat{x}_j^-)(\hat{x}_j^+ - \hat{x}_j^-)^T \] (27)

Suppose that (24) alternatively represents the updated covariance of SVSF. It is totally same with Kalman Filter, then (26) can be approximately reformed as
\[ \hat{Q} = K_k^{SVSF} C_k K_k^{SVSF^T} \] (28)

### 3.2. Adaptive covariance matrix of measurement noise statistic

Similarly, since \( Q \) is fixed and independent of \( \alpha \), then (18) becomes
\[ \sum_{j=k-N+1}^{k} \text{tr}\left\{ C_j^{-1} - C_j^{-1} d_j d_j^T C_j^{-1} \right\} [0 + I] = 0 \] (29)

It can also be simplified as
\[ \sum_{j=k-N+1}^{k} \text{tr}\left\{ C_j^{-1} C_j - d_j d_j^T \right\} C_j^{-1} = 0 \] (30)

then by deriving (30), it yields
\[ C_k = \frac{1}{N} \sum_{j=k-N+1}^{k} d_j d_j^T \] (31)

Now since \( \frac{1}{N} \sum_{j=k-N+1}^{k} d_j d_j^T \) is the way to calculate the expectation of \( d_j d_j^T \), which is also as shown in (2), then the recursive measurement error covariance matrix is
\[ \hat{R} = C_k - H P_{k|k-1} H^T \] (32)

Mathematical derivation above showing that the adaptive covariance matrix of measurement noise statistic seems able to be adopted from the value used at the previous iteration. Finally, both the process and measurement noise statistic are obtained already when their corresponding mean are considered to be zero.
4. ADAPTIVE SVSF-BASED FEATURE 2D SLAM ALGORITHM

The proposed method is approached to address a feature-based SLAM problem of the wheeled mobile robot [14, 17]. The objective is concurrently estimating the robot pose and feature in certain environment. It is assumed that by using the motion model the robot moves after executing the control command, and by using laser scanner-based measurement, it senses the features with distance and bearing as the gathered data [3, 4, 43, 44]. It is noted that all the prerequisites for a feature-based SLAM algorithm in [14] and [17], therefore,

Algorithm 1 ASVSF-SLAM Algorithm

1. Loop
2. Prediction Step: If proprioceptive data is available
3. Propagate the state estimate \((3)\)
4. Propagate the covariance relative to the state \((4)\)
5. Update Step: If the observation data is available
6. Compute the innovation sequence error \((5)\)
7. Calculate Gain \((9)\)
8. Update the State, and Covariance \((10) and (11)\)
9. Compute the noise statistic \((28) and (32)\)
10. endloop

5. RESULTS AND DISCUSSION

The proposed algorithm discussed above is realistically simulated and applied for solving SLAM problem of wheeled mobile robot. Initially, the robot pose and covariance as well as all the completeness parameters for ASVSF are initialized as follows

\[
\hat{x}_0 = \begin{bmatrix} 0 \\ 0 \\ \frac{d_{ls}}{180} \end{bmatrix}, \quad P_0 = \begin{bmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{bmatrix}, \quad \gamma = 15e - 2, \quad e_{z,0} = \begin{bmatrix} 0.1 \\ \frac{0.5\pi}{180} \end{bmatrix}^T
\]

Note that all the parameters shown herein are adopted from the real robot platform, Turtlebot2, which equipped with laser scanner [4, 43, 14] in displacement \(d_{ls} = 14\, \text{cm}\). By realistically measuring the distance between two separately powered wheels, it is obtained \(W_r = 33\, \text{cm}\). It assumed that this mobile robot is operated in planar indoor environment with the size and random point as described in Figure 1 that is served as the reference path and map in this experiment. The validation is conducted based on RMSE of different algorithm in estimating the robot path and map.

Figure 1. Reference trajectory and map
The validation is conducted based on RMSE of different algorithm in estimating the robot path and map. There are two different condition of the initial noise statistic in order to see the consistency of the proposed algorithm as shown in Table 1. All the parameters presented in Table 1 aim to know the performance of the proposed algorithm when the initial process and measurement noise statistic are increased in type of additive white Gaussian noise.

| No. | \( r_0 \) | \( \hat{r}_0 \) | \( q_0 \) | \( \hat{q}_0 \) | \( Q_0 \) |
|-----|-----------|-----------|---------|---------|---------|
| 1st Simulation | 0.5 \( 5\pi/180 \) | 0 \( 5\pi/180^2 \) | 0.05 \( 2\pi/180 \) | 0 \( 2\pi/180^2 \) |
| 2nd Simulation | 0.8 \( 8\pi/180 \) | 0.8 \( 8\pi/180^2 \) | 0.1 \( 8\pi/180 \) | 0 \( 8\pi/180^2 \) |

All the parameters presented above aim to know the performance of the proposed algorithm when the initial process and measurement noise statistic are increased in type of additive white Gaussian noise. The scenario is involved to validate the stability of the proposed ASVSF-SLAM algorithm compared to conventional SVSF-SLAM algorithm. Regarding to these parameters and the reference path depicted in Figure 1 the following results were obtained. It analogized that the robot moves based on all the command send to the odometers. It aims to track the reference path as well as locating new detected landmark in the environment then by applying two different algorithm which are SVSF-SLAM and Adaptive SVSF-SLAM algorithm, the performance of the robot can be graphically expressed as shown in Figure 2.

Figure 2 represents the performance of different SLAM algorithm. They are attempted to estimate the path and map coordinate by respecting to the reference trajectory. According to different simulations, both SVSF and ASVSF-based SLAM algorithm show the convergence to track the reference. Additionally, the proposed method shows a smoother performance with a guaranteed stability when the noise statistic is increased. However, it is quite difficult to know the detail diversity of the SLAM algorithms through the graphical representation only.

Therefore, to ease the validation and analysis, their estimated path and estimated map coordinate are compared in term of root mean square error. Figure 3 depicts the difference RMSE values for SVSF and ASVSF-SLAM algorithms. According to two different simulation, it is clear to see that the adaptive SVSF gives smaller RMSE for the estimated robot path in which there is no much diversity to its reference. By using the same method and term, the estimated map of SVSF and ASVSF-SLAM algorithm is also compared.
According to Figure 4 the stability and accuracy of ASVSF-SLAM is validated. There is no significant effect after increasing the initial noise statistic. Therefore, it can be stated that since no degradation detected, ASVSF-SLAM algorithm is better than SVSF-SLAM algorithm.

Figure 3. RMSE of estimated path coordinate for (a) 1st simulation and (b) 2nd simulation

Figure 4. RMSE of estimated path coordinate (a) 1st Simulation and (b) 2nd Simulation

Referring to all the graphical result above, it might be difficult to see the difference. For this reason, the following Tables 2 and 3 are presented. In which, these tables are intended to give detail values for all test as the way to validate the accuracy for each algorithm.

### Table 2. RMSE of different SLAM-based algorithm (first test)

| SLAM Alg. | x-EPC (cm) | y-EPC (cm) | θ-EPC (rad) | x-EMC (cm) | y-EMC (cm) |
|-----------|------------|------------|-------------|------------|------------|
| SVSF      | 6.4992     | 11.2050    | 0.1066      | 16.1687    | 20.0962    |
| ASVSF     | 5.6514     | 2.6893     | 0.0991      | 11.1031    | 12.1210    |

### Table 3. RMSE of different SLAM-based algorithm (second test)

| SLAM Alg. | x-EPC (cm) | y-EPC (cm) | θ-EPC (rad) | x-EMC (cm) | y-EMC (cm) |
|-----------|------------|------------|-------------|------------|------------|
| SVSF      | 11.3148    | 19.2975    | 0.7886      | 31.3384    | 38.7499    |
| ASVSF     | 5.5325     | 6.4678     | 0.1109      | 24.9880    | 29.7186    |

### 6. CONCLUSIONS

The main contribution of this paper is to equip the traditional SVSF with an approach termed as adaptive filtering strategy. It utilizes the maximum likelihood estimation (MLE) used to approximate the error covariance matrices of noise statistic by conditioning the probability density function of measurement to an
unknown parameter at one iteration. The output of this project is the enhancement of SVSF. It can recursively calculate the covariance of the noise statistic based on the uncertainty condition of the previous process. In other words, the predetermined covariance of the noise statistic is executed once at the first iteration and the system continuously generates new covariances for the rest iteration. The proposed method is applied to solve the feature-based SLAM problem of a wheeled mobile robot named ASVSF-based SLAM algorithm. The presence of adaptive strategy prevent the SVSF from degradation and divergence condition under time integration when it is applied for the real case. Regarding to all the comparative results, the accuracy, stability, and robustness of the proposed algorithm is guaranteed and satisfied.

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BIOGRAPHIES OF AUTHORS

Heru Suwoyo is lecturer at Department of Electrical Engineering, Universitas Mercu Buana, Indonesia. Currently, he is a Ph.D. candidate at Department of Mechatronic Engineering, School of Mechatronic Engineering and Automation, Shanghai University, China. His research interest include Mobile Robot Navigation, Simultaneous Localization and Mapping, Fuzzy Logic Controller, Probability-Based Filtering Method such as Extended Kalman Filter and Smooth Variable Structure Filter, Adaptive-Filtering and Population-Based Metaheuristic Optimization such as Ant Colony Optimization, Genetic Algorithm and Particle Swarm Optimization.

Yingzhong Tian is an associate professor now and also is the Director of Research in LIMAR (Lab of Intelligent Mechanism and Advanced Robot) research team in Shanghai University. He obtained a Ph.D. degree in Mechanical manufacture and automation in 2007 from Shanghai University. His research interests include mobile robot, bionic robot, multi-robot systems and image processing.

Wenbin Wang obtained a Ph.D. degree in Mechanical manufacture and automation in 2007 from Shanghai University. Now, he is working in Shen Zhen Polytechnic as an associate professor. His research interests include image processing, soft robot, industry robot and application.
Long Li is a member of LIMAR (Lab of Intelligent Mechanism and Advanced Robot) research team in Shanghai University. He obtained a Ph.D. degree in Mechanical Design and Theory in 2013 from Harbin Institute of Technology (HIT). His research interests include mobile robot, bionic robot, soft robot and multi-robot systems.

Andi Adriansyah is lecturer at Department of Electrical Engineering, Universitas Mercu Buana, Indonesia. He obtained Ph.D. degree in Electrical Engineering from Universitas Teknologi Malaysia, Malaysia in 2007. His research interest includes Mobile Robot Navigation, Soft Robotics, Closed-Loop Controller such as PID and FL Controller, Heuristic Algorithm-Based Tuning Method, and Artificial Intelligent.

Fengfeng Xi is the director of the Ryerson Institute for Aerospace Design and Innovation (RIADI), which connects undergraduates to leading Canadian aerospace companies. His research interest includes designing smart aircraft cabins and seats, and aircraft manufacturing automation. He is also engineering a wing that morphs to adapt to different conditions, making air travel more fuel efficient.

Guangjie Yuan is a member of LIMAR (Lab of Intelligent Mechanism and Advanced Robot) research team in Shanghai University. He obtained a Ph.D. degree in Materials Engineering from University of Tokyo, Tokyo, Japan, in 2014. His research interests include micro-nano manufacturing, sensors for robot, and bionic robot.