Mechanical Response of PbSSe, PbSTe Ternary and PbSnSTe Quaternary Alloys at High Pressure

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Abstract—Property of the semiconductors under high pressure is investigated by the density functional theory and paralleled to the foretelling of the linear elasticity theory. In addition, ternary alloys of PbS,Se x, and PbS,Te x, lattice matching PbS substrate for x = 0.5 compositions are studied. Furthermore, quaternary alloys PbSn,S,Te x, lattice matching PbS substrate for x and y = 0.5 compositions are studied. The six independent elastic parameters (Cij) are also calculated. Meanwhile, the results data are analyzed in high pressure. The mechanical response of all alloys to pressures 0, 50 and 100 kbar increases progress to decrease in (Cij) in separate rates. The rapprochement between the calculated results and the available published data for these alloys demonstrate that they had worthy accordance at zero pressure and the results at high pressure may be required as an acceptable reference.

Index Terms—Alloys, High pressure, Mechanical response, PbSSe, PbSTe, PbSnSTe.

I. INTRODUCTION

The study of the mechanical response of materials is significant in both the fundamental physics and high-pressure technique. The selection of the mechanical response under pressure is extremely risky by theoretical simulations. A strong connection exists between these properties with shear rigidity of materials and with their elastic moduli (Suresh Babu, Vijayan and Devanathan, 2004). The technical significance of the PbS and PbSSe groups of semiconductor compounds and alloys as detectors of infrared radiation has been a powerful parallel stimulus. They are chiefly used in infrared lasers in fiber optics, including thermoelectric materials, in solar energy panels, and in window coating (Othman, Mishjil and Habubi, 2012; Othman, et al., 2019). Their narrow fundamental energy band gap is one of their effective properties (Gopal, et al., 2014). Countless studies, theoretically and experimentally, related to these materials are available (Lebedev and Shluchinskaya, 1994) and explored the samples of PbS,Se x,Te 1-x-y quaternary solid solutions at low temperatures using electrical and X-ray methods (Weyand, 2007); ab initio study of cubic alloys (Kacimi, et al., 2008); structure, electronic, and optical properties of PbS,Se x (Labidi, et al., 2011); and simulation mechanical properties of PbS,Se 0.5 under pressure (Othman, 2013). The existent study was performed to highlight on the studies which are done in the future by the specialists to deliver and examine these alloys in laboratories. It assists them determine the change in amounts of additives in alloys, the friendship of theoretical studies with experiments and other theoretical works.

The mechanical performance of PbS,Se x, and PbS,Te 1-x ternary, PbSn,S,Te x,y quaternary alloys high pressure for x and y = 0.5 compositions changes under pressure, which in a straight line impact a variety of applications of PbS compound devices under diverse working circumstances. Concerning various application circumstances, the mechanical performance of these alloys at 0, 50, and 100 kbar is considered using density functional theory (DFT) calculations in the current work.

II. MATERIALS AND METHODS

Cambridge Serial Total Energy Package (CASTEP) program is used to analyze the data (Segall, et al., 2002). Kohn–Sam formation is used to complete the calculation (McGinty, et al, 2009). Using DFT to the exchange-correlation contribution is explained within the local density approximation (LDA). A cubic unit cell is centered with atoms (S/Se) and (S/Te) of PbS,Se x, and PbS,Te 1-x ternary alloys and set up with atoms (Pb/Sn) and (S/Te) of PbSn,S,Te x,y quaternary alloys for x and y compositions. It is indicated that quaternary alloys have cubic symmetry in all of the calculations for all the five systems to preserve constancy and easiness. Cubic unit cell was taken for x and y and we substituted atoms to achieve the coveted concentrations. The completion of the first step of geometry optimization is done for PbS,Se x,y, and PbS,Te 1-x,y ternary alloys and PbSn,S,Te x,y quaternary alloys for x and y = 0 at constant temperature with symmetry P1. Fig. 1 displays the graph of improvement steps provided merely for PbSn,S,Te 1-x,y quaternary alloys to gain gap in journal. The calculation is perfected using Kohn–
Sam formation, which used DFT to the exchange-correlation contribution. It is determined by LDA. The wave functions have been extended in the plane waves up to a kinetic energy cutoff of 890 eV. Atomic positions are adjusted with a density mixing scheme (Othman, Kasap and Korozlu, 2010a) including the conjugate gradient (CG) process for values minimization (Ahmed, et al., 2008). Under dissimilar pressure, the Monkhorst-Pack scheme with regular integration points is put in an application (Milman, et al., 2010; Sedighi, et al., 2020).

III. RESULTS AND DISCUSSION

Below are the elements which acted the external forces in mechanical performance. They are also called stress. In addition, whereas the body is in equilibrium, the external stress has to be perfectly well adjusted by internal forces. Overall, the stress is a second rank tensor with nine following in some references, stated by the three column vectors $a_i$, $b_i$, and $c_i$ in the distorted state, the strain tensor is expressed by:

$$\tau = \frac{1}{T} \left( \sum_{i=1}^{N} m_i \left( v_i v_i^T \right) + \sum_{j} \eta_{ij} F_{ij}^T \right)$$

where index indicates particles 1 by means of $N$, $\eta_{ij}$, $v_i$, and $F_{ij}$ symbolize the mass, velocity, and force working on character $i$, $\theta$ means the arrangement volume. Application of a stress of body brings about a modification in the relative positions of particles in the body, directed quantitatively by way of the strain tensor:

$$\eta_{ij} = \begin{bmatrix} \eta_{11} & \eta_{12} & \eta_{13} \\ \eta_{21} & \eta_{22} & \eta_{23} \\ \eta_{31} & \eta_{32} & \eta_{33} \end{bmatrix}$$

parallelepiped (e.g., a periodic simulation cell) categorized in some references, stated by the three column vectors $a_{i\theta}$, $b_{i\theta}$, and $c_{i\theta}$ and by the vectors $a$, $b$, and $c$ in the distorted state, the strain tensor is expressed by:

$$\eta = \frac{1}{2} \left[ \left( P_0^T \right)^{-1} K P_0^{-1} - 1 \right]$$

where $P_\theta$ points to the matrix formed from the three column vectors $a_{i\theta}$, $b_{i\theta}$, and $c_{i\theta}$, $P$ signifies the corresponding matrix formed from $a$, $b$, and $c$. $T$ indicates the matrix interpret. $K$ means the metric tensor $P^T P$. The elastic hardness coefficients concerning the various components of stress and strain are defined by:

$$C_{imnk} = \frac{1}{\eta_{imk}} \left( \frac{\partial^2 A}{\partial \eta_{imk} \partial \eta_{nk}} \right)_{\eta_{imk} = 0}$$

where $A$ stands for the Helmholtz which releases energy. For small deformations, the affiliation between the stresses and strains may be stated basing on a popularized:
strain patterns with changing amplitudes and a subsequent calculation of the stress tensor after optimization of the internal structure parameters. In addition to that, the bulk modulus $B$ is calculated from the elastic constants. Then, Young’s modulus is computed from these values.

Table I displays lattice parameter of PbS$_x$Se$_{1-x}$ and PbS$_x$Te$_{1-x}$ ternary and Pb$_x$Sn$_{1-x}$S$_y$Te$_{1-y}$ quaternary alloys for $x$ and $y$ compositions with increasing pressure ($P = 0.50$, and 100 kbar). These lattice parameters decline, as pressure rises. Moreover, whereas forbidden band gap energy goes up because of the pressure. For further information, as pressure increases, many of materials often get metallic. Furthermore, the atoms come closer, and the lattice parameter goes down. Thus, all modulus enlarge. Eventually, the referred materials get metallic than the pressure decreases (Koch, et al., 2005). A connection is provided between the mechanical characteristic of crystals by the elastic parameters of materials, which display information in terms of the nature of the forces operating in materials. Particularly, they give information about the materials’ constancy and rigidity. Accurate ways and means must be applied to their first principle calculation. Since these forces and the elastic parameters are considered as the functions of the first-order and second-order derivatives of the potentials, the calculation demonstrates more detail about the accuracy of forces in materials. The second-order elastic parameters ($C_{ij}$) are done by means of the “volume-conserving” proses (Sanati, et al., 2013) and the findings are indicated in Table II. For a stable tetragonal structure, the six independent elastic constants $C_{ij}$ should gratify the Born-Huang for constancy (Mouhat and Coudert, 2014),

$$C_{ij} > 0, \quad C_{11} > 0, \quad C_{44} > 0, \quad C_{66} > 0, \quad (C_{11} - C_{12}) > 0, \quad (C_{11} + C_{33} - 2C_{13}) > 0,$$

$$\{2(C_{11} + C_{12}) + C_{33} + 4C_{13}\} > 0$$

Table II indicates that elastic constants follow the stability conditions for PbS$_x$Se$_{1-x}$ and PbS$_x$Te$_{1-x}$ ternary and
S_{x}Te_{1-x} quaternary alloys for x and y = 0.5 as a function of pressure from 0, 50, and 100 kbar are demonstrated in Figs. 3 and 4.

In the final analysis, whereas the pressure rises, the parameters vary regularly. It displays that the varying of bulk modulus with pressure of PbS_{x}Se_{1-x} alloys decreases quickly and the varying of bulk modulus for PbSxTe_{1-x} alloys decreases gradually with the pressure. As can be noted in Fig. 3, quaternary alloys of PbSn_{x}S_{1-x}Te_{1-y} bulk modulus decrease regularly. It can be indicated as one of the key references for the other works in the future. In Fig. 4, the young modulus parameters decline, as pressure goes up, but the varying of bulk modulus rises with the pressure in PbSxTe_{1-x} alloys.

**IV. Conclusions**

The current study indicates the mechanical performance of PbS_{x}Se_{1-x} and PbS_{x}Te_{1-x} ternary and PbSn_{x}S_{1-x}Te_{1-y} quaternary alloys for x and y = 0.5 as a function of the pressure from 0, 50, and 100 kbar using DFT. The first principles method is used to achieve the results depending on the LDA using plane wave pseudopotentials. The traditional mechanical stability conditions for these ternary and quaternary mixed crystals are satisfied by the elastic parameters. The pressure increasing leads to a decrease in the lattice parameters. Moreover, parameter bulk and young modulus go down with pressure increasing, but young modulus parameters of PbS_{x}Te_{1-x} ternary go up by pressure. The results display the calculation of C_{ij} of all alloys as a pressure from 0, 50, and 100 kbar. Pressure increasing progress to decrease in C_{11}, C_{11}, and C_{12}, and in C_{11}, C_{44}, and C_{66} in separate rates. The data of the current study include P = 50 and 100 kbar, and it can be emphasized on in the future studies.

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