The proton conductivity in benzimidazolium azelate under moderate pressure

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Abstract

The kinetic Monte Carlo method is applied to examine effects of hydrostatic pressure on the benzimidazolium azelate (BenAze) proton conductivity. Following the experimental indications the recently proposed model has been modified to simulate the transport phenomena under moderate pressure, resulting in a very good agreement between numerical and experimental results. We demonstrate that the pressure-induced changes in the proton conductivity can be attributed to solely two parameters: the length of the hydrogen bond and the amplitude of lattice vibrations while other processes play a more minor role. It may provide an insight into tailoring new materials with improved proton-conducting properties. Furthermore, in high-pressure regime we anticipate the crossover from the increasing to decreasing temperature dependence of the proton conductivity resulting from the changes in the hydrogen-bond activation barrier with increased pressure.

Keywords: Anhydrous proton conductor, Heterocyclic-based compounds, High pressure, Kinetic Monte Carlo
I. INTRODUCTION

Proton conductivity is a very interesting transport phenomenon involved in the long-range charge transfer mechanism. The recent great interest in proton transfer unassisted by water comes from the search for fuel cells operating above the boiling point of water (373 K) but below extremely high temperatures typical for solid oxides. One possibility is to create the proton conductor on the basis of heterocyclic compounds [1, 2] that display many characteristics to water: they are amphoteric, undergo autoprotolysis and possess the ability to form hydrogen bonds. And most importantly, they have substantially higher melting points (e.g.: benzimidazole—447 K). Based on these properties various proton conductors, both the polymer [3–7] and crystalline [8, 9] can be created. In recent years we have focused on the dicarboxylic acid salts family. Such crystalline anhydrous proton conductors are organic molecules formed with heterocyclic nitrogen-containing organic chains of imidazole, triazole and benzimidazole and dicarboxylic acids. These compounds have a number of structural similarities: the chains which are formed from acids and heterocyclic molecules are linked by hydrogen bonds while the layers are stabilized by the weak electrostatic interaction. In general the proton conductivity increases with temperature according to the Arrhenius law which indicates the dominant character of the Grotthuss mechanism [10, 11].

Proton conductivity of anhydrous heterocyclic molecules based materials is a complex process affected by many external factors, e.g. temperature and pressure. An external pressure affects the length of the hydrogen bonds and modifies the mobility of the structural elements involved in the process. In the literature, the effect of pressure on proton conductivity is analyzed mainly for materials exhibiting phase transition to the highly conductive phase (superprotonic), for example, CsHSO$_4$ [12] or [(NH$_4$)$_x$Rb$_{1-x}$]$_3$H(SO$_4$)$_2$ [13, 14]. The application of the hydrostatic pressure causes an increase in the thermal stability of the superprotonic phase [13]. This is mainly due to an increase in the melting point, while the phase transition temperature varies slightly with an applied pressure. The similarity of the $p$–$T$ phase diagrams of compounds belonging to the $M_nH_n(XO_4)_{(m+n)}/2$ class of proton conducting crystals (where $M = K$, Cs, Rb, NH$_4$ and $X = S$, Se) suggests also the possibility of inducing the superionic phase even at the absence of the normal atmospheric pressure conditions [15, 16].

The electric properties and molecular dynamics of BenAze at ambient pressure have been
studied experimentally by Zdanowska-Frączek at al. [17, 18]. The studies revealed that the temperature dependence of proton conductivity can be fitted to the Arrhenius law and the proton conduction is well described by the Grotthuss-type diffusion mechanism. Moreover, a detailed description of the proton migration path was proposed [18]. The proton conductivity studies performed at different thermodynamic conditions [17–20] disclosed that BenAze is extremely sensitive to external pressure. In particular, the proton conductivity values decrease with increasing pressure and the significant change of the conductivity characteristics shape is observed from linear (an Arrhenius-type behavior) to nonlinear ones. However, a scaling procedure between the ac conductivity, dc conductivity, current frequency and pressure (proposed by Sommerfield [21]) leading to one master curve for various temperatures at ambient pressure is well preserved also for different pressures at a fixed temperature [17]. This indicates the presence of the same mechanism responsible for proton conductivity at various thermodynamic conditions.

Therefore, we have attempted to support the experimental results observed at elevated pressures by microscopic model simulations. The theoretical model describing the proton transport in accordance with the Grotthuss mechanism has been presented recently [22]. For the pure benzimidazole, where the benzimidazole molecules form a long chain connected to one another by hydrogen bonding, the numerical results were in very good agreement with experimental measurements. However, the structure of BenAze made of infinite azelaic acid anion chains connected with benzimidazolium cations by hydrogen bonds is much more complex. Therefore, based on the experimental indications our model has been modified to reproduce the essential features of BenAze conductivity including the influence of hydrostatic pressure.

The theoretical simulations supported by experimental data presented in our paper should provide significant input into the understanding of the source of the proton conductivity. Furthermore, some practical conclusions are drawn for the high pressure range that has not yet been studied experimentally.

The paper is organized as follows: in Sec. II we present the microscopic model to study effects of moderate hydrostatic pressure in BenAze. In Sec. III the simulation results are presented and discussed. Finally Sec. IV concludes our paper, summarizing the main findings.
II. THE PROTON CONDUCTIVITY MODEL OF BENAZE

Recently we have proposed a microscopic model of the proton conductivity based on the kinetic Monte Carlo (KMC) approach\cite{22} adequate to characteristic time scales for the proton conduction\cite{23}. The KMC method yields time evolution of the system provided that all transition rates from every configuration to every other allowed state are known\cite{24}. If we count protons crossing a specified position in the chain then we are able to calculate the proton current. For the polycrystalline benzimidazole a proton conduction path was modeled by a chain of parallel rigid rods whose ends can be occupied by protons. Benzimidazole molecules modeled as rods can rotate by $180^\circ$ flip with or without protons. Protons are also able to migrate by hopping from one rod to the nearest one provided the end of the adjacent rod is empty.

It is well established that application of pressure impacts the proton dynamics. The hydrostatic pressure reduces the atomic volume of a substance and promotes closer packing of atoms (ions) actually modifying the proton transfer both through an H-bond and by a rotation. The question arises if either of these processes become prevailing when a moderate hydrostatic pressure is present. According to Fig. 1 there are two noticeable effects of increasing pressure: the proton conductivity decreases and the range of conductivity values is getting narrower. One might suppose that the reduction of rotations at elevated pressure, as a consequence of the increasing activation energy, may be responsible for both issues. However, our previous simulations\cite{22} demonstrated that the proton current behavior strongly depends on the ratio of the hop frequency to the rotation frequency resulting in two distinct regimes with significantly different behavior. As shown, the linear dependence of the proton current on the relative frequency takes place in the rotation-dominated regime whereas the current saturates within a broad relative frequency range in the hopping-dominated regime. So, if the decrease of the rotation frequency is not accompanied by a change in the hopping frequency, both effects of increasing pressure cannot occur simultaneously. Therefore, when the pressure-driven modifications of the H-bond potential have turned out to be essential, it is worth checking whether the changes in rotations are required to the same extent.

As far as modifications of the H-bond potential are concerned a typical dependence of the pressure on the anionic group distance is nonlinear\cite{25,26}. So, it can be expected that for a higher pressure the average distance between the benzimidazoles decreases slower.
than linearly. Another very important effect of pressure is a nonlinear decrease of the amplitude of lattice vibrations resulting from a damping out the mechanical oscillations by internal friction [26,28]. When the perturbation theory is employed, the third order elastic constants are required to determine the high pressure dependence of the lattice vibrations [26].

Crucial for our considerations is that BenAze proton transfer path consists of three different types of hydrogen bridges [17]. Namely, there are O–H···O (2.54 and 2.56 Å), N–H···O (2.64 and 2.72 Å) and N–H···N (2.732 and 2.651 Å) bonds. It can be assumed that the entire conduction process is limited by the longest hydrogen bond N–H···N. It has the highest H-bond barrier and then the lowest conductance. Moreover, the energetically favored N–H···N angle is close to 180° meaning the H-bond is almost linear [29] and can successfully be modeled by one-dimensional potential [22].

Without precise experimental data, we are not able to examine the remaining elements of the transfer path in detail. But we can propose a simple theoretical model which exploits the existence of the “bottleneck bond”. We use the black-box concept replacing all other processes (the remaining tunnelings, trans-gauche motion of azelate acid chains and benzimidazole flips) by a single effective process. Its basic function, as for a rotation in the Grotthuss mechanism, is to supply a proton to the longest N–H···N bond with a certain frequency. In this way, the cooperative character of the proton transport, the structural reorganization and proton migration along the H-bonds, has been taken into account.

As the amphoteric nitrogen-based heterocycles demonstrate the presence of both protonated and non-protonated nitrogen atoms they can act as donors and acceptors in proton-transfer reactions. For the realistic system the concentration of protons on the benzimidazole molecule is slightly shifted from the half-filled case because of various crystal structure imperfections. In our simulations the proton concentration is defined by the ratio $c = n/(2N)$, where $n$ is the number of protons and $N$ is the number of rods. As there is no indication from the experiment the effective concentration was chosen arbitrarily as $c = 0.49$. As we have checked, a change in the effective concentration of a few percent does not change the results qualitatively.

We approximate the H-bond potential by the back-to-back Morse functions spanned between the nitrogen anions where the parameter $d$ represents the distance between them.
The larger \( d \) the stronger H-bond potential.

\[
V_a(x) = \frac{1}{2a} \int_{-a}^{a} \left[ V_{\text{Morse}} \left( \frac{d}{2} - x + y \right) + V_{\text{Morse}} \left( x - y - \frac{d}{2} \right) \right] dy ,
\]

\[
V_{\text{Morse}}(x) = g \left[ \exp \left( -\frac{2x}{b} \right) - 2 \exp \left( -\frac{x}{b} \right) \right] .
\]

The hopping between the H-bond minima is defined as the thermally assisted tunneling. In order to model the effect of lattice vibrations at a reasonable computational cost we assumed that the position of the nitrogen anions are fuzzy. As a consequence, the parameter \( a \) responsible for the dispersion in the position of the anions appears in the above formula. Due to vibrations the Morse potential barrier is lowered effectively and a current flows more easily. More details about the model can be found in [22].

### III. RESULTS AND DISCUSSION

At ambient pressure the \( \sigma_{\text{dc}} \) conductivity of the BenAze sample [17], calculated from its bulk resistance, one may try to approximate by the Arrhenius law. However, at elevated pressure the experimental results departure significantly from such a behavior (see Fig. 1). In order to determine the best-fitting parameters the KMC results have been compared

![Figure 1](image-url)

Figure 1. The temperature-dependent dc conductivity for BenAze at various pressures. Dashed lines connect the experimental points: pluses – 0.1 MPa, triangles down – 109 MPa, crosses – 155 MPa, triangles up – 250 MPa. Solid lines represent KMC simulations, whereas dotted lines come from the KMC predictions at 390, 525 and 725 MPa, respectively.
simultaneously with available experimental data apart from the measurements for a pressure of 0.1 MPa. In the latter case the black-box approximation seems to be too rough because some additional microscopic effects are likely to be significant in the low pressure regime. The best fit parameter values are presented in Table I.

Table I. Values of model parameters. The definitions of parameters and symbols are the same as in our previous paper [22].

| Parameter                          | Symbol | Value          |
|------------------------------------|--------|----------------|
| Frequency of rotation prefactor    | $\nu_R^{0}$ | $7.5 \times 10^7$ Hz |
| External electric field            | $K$   | 0.01 V/Å       |
| Bond length                        | $d_0$ | 2.73 Å         |
| Thermal expansion coefficient      | $d_1$ | 0.0004 Å/K     |
| $V_a$ barrier height               | $h(T_0)$ | 0.8 eV        |
| Distance between minima of $V_a$   | $\Delta x(T_0)$ | 0.713 Å     |
| Reference temperature              | $T_0$ | 313 K          |
| $D$ and $L$ defects energy         | $V_{Coul}$ | 0.2 eV       |
| Frequency of hopping prefactor     | $\nu_T^{0}$ | $10^9$ Hz   |
| Lattice vibration amplitude        | $a_0$ | 0.25 Å         |
| Thermal susceptibility of $a$      | $a_1$ | 0.0033 Å/K     |

The basic model assumptions have been chosen to satisfactorily reproduce in the KMC simulations the experimental data for moderate pressures. This implies a tolerable reproduction of experimental measurements at ambient pressure. Such a procedure is dictated by the assumption that because of the loose structure of BenAze the black-box should work better at higher pressure. In accord with our expectations the $d(p)$ and $a(p)$ functions (the H-bond potential parameters) have turned out to be nonlinear and monotonic (see Fig. 2). Moreover, since the damping, as a bulk phenomenon, weakly depends on the material structure the potential parameter $a$ varies smoothly under pressure. In contrast, the pressure compression of bond lengths is more complex and likely only for higher pressure curves would become really smooth.

Despite the fact that we have experimental data only for three moderate pressures, we may give some predictions about what can be expected for pressures higher than the reported
Figure 2. The crosses represent the H-bond potential parameters, $d$ and $a$, at $T = 313$ K obtained from the best fits of the dc conductivity data. The dotted lines are a guide for the eye. The pluses denote the same H-bond potential parameters extrapolated from the exponential fit to higher pressures at 390, 525 and 725 MPa. The corresponding proton conductivities are demonstrated in Fig. 1.

ones [17]. For this purpose, $d(p)$ and $a(p)$ curves were extrapolated up to 800 MPa using an exponential decay function which should give a qualitatively correct fit. The fit included only data for 109, 155 and 250 MPa, as the ambient case could distort the predictions because of the loose structure of BenAze. The other model parameters for the elevated pressures are the same as in Table I.

As the points for experimentally examined pressures lies fairly well on the fitted curves for $d(p)$ and $a(p)$ we may expect that the assumptions we made should work for some higher pressure. The rotational frequency, $\nu_0^R$, at higher pressure may decrease as rotations are hindered but the assumption that it may be approximated by a constant value in a wide range, as it is for 100–250 MPa, should still be valid. Thus, the predictions presented in Fig. 1 should not be disturbed, at most they could be shifted down.

The three exemplary curves in Fig. 1 show the pressure evolution of the thermal conductivity and the crossover effect is firmly established. In the interval 500–550 MPa the current becomes almost constant with temperature while above this value the proton conductivity, contrary to expectations, starts to decrease with increasing temperature. For pressure lower than 390 MPa the H-bond barrier decreases with increasing temperature whereas for higher pressures the behavior of H-bond potential starts to reverse gradually. In the interval 500–550 MPa the shape of H-bond potential is almost frozen for all examined temperatures. At 725 MPa the process of reversal is finished and above the H-bond potential barrier increases
with increasing temperature. The explanation may be brought directly from the definition of $V_a(x)$ potential that declines with decreasing $d$ but grows with decreasing $a$. Thus, the conductivity behavior with increasing pressure is a result of the interplay of $d$ and $a$. It occurs that for BenAze the decline of $a$ wins with the effect of decreasing $d$ resulting in behavior shown in Fig. 3 and further in Fig. 1. Also, the evolution of thermal behavior of hydrogen bonding can be based on the analysis of the thermal dependence of $d$ and $a$ parameters. We consider the linear approximation, i.e.:

$$
\begin{align*}
    d(T) &= d_0 + d_1 (T - T_0), \\
    a(T) &= a_0 + a_1 (T - T_0)
\end{align*}
$$

and assume that the both linear coefficients, $d_1$ and $a_1$, retain the mutual relationship of the potential parameters shown in Fig. 2. Naturally, the values of $d_0$, $d_1$, $a_0$ and $a_1$ must be in the proper proportions to give the behavior presented in Fig. 1. Otherwise, for example, the conductivity curves could be concave instead of convex.

Figure 3. The evolution of H-bond potential with increasing pressure plotted between the minima. a) A typical behavior for lower pressures, $V_a(x)$ for 109 MPa is given as an example; b) At 390 MPa the inversion of potential curves with the temperature ordering starts; c) 525 MPa – the point where the potential very weakly depends on the temperature; d) Above 725 MPa the potential grows with the temperature in the considered range.

In general, the proton conductance of various materials can change substantially with temperature and pressure. At the level of the microscopic description, as shown by our discussion, the crucial point is the interplay between only a few parameters: bond length $d_0$, thermal expansion coefficient $d_1$, lattice vibration amplitude $a_0$ and lattice vibration
thermal susceptibility $a_1$. This may serve as an indication of promising compounds among those exhibiting a low proton conductivity at ambient pressure. Some of them can manifest as a considerable increase in the conductivity at higher pressures related to the lowering of the activation barrier. We hope that this knowledge will help technologists to successfully design new materials to be used in electrochemical devices.

IV. SUMMARY

BenAze belongs to the wide family of organic acids with heterocyclic molecules. Its conductivity is too low for practical applications but in view of the well-known crystalline structure it can serve as an excellent system for testing. The proton transport efficiency in BenAze is controlled by the longest N–H⋯N hydrogen bonds playing the role of bottlenecks. In our simulations the proton migration along this H-bond was analyzed thoroughly while all other transport sub-processes (rotations, tunnelings) were replaced by a single effective process with a fixed frequency. The simulation results were found to be in good agreement with the experimental data indicating that the basic model assumptions have been chosen properly in a wide range of thermodynamic parameters.

The present simulations confirm a sequence specificity of the proton motion via the Grotthuss mechanism. The pressure-induced changes in the proton conductivity have occurred to be attributed to solely two parameters: the length of the hydrogen bond and the amplitude of lattice vibrations indicating the dominant role of hydrogen bonds in the proton transport under moderate pressure. It agrees with the hypothesis that in the proton conductors exhibiting a Grotthuss-type mechanism [30, 31] the proton hopping across the hydrogen bond rather than the transfer due to reorientational motions is the rate-limiting step.

Based on our simulations we postulate the existence of the crossover in the thermal conductivity above pressures examined in the experiment. The key to understanding the pressure-driven inverse of the monotonicity of the proton conductivity is the behavior of the hydrogen-bond activation barrier with increased pressure. Experimental verification of our supposition has been scheduled for further studies.
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