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Absolute Asymmetric Synthesis Involving Chiral Symmetry Breaking in Diels–Alder Reaction

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Abstract: Efficient generation and amplification of chirality from prochiral substrates in the Diels–Alder reaction (DA reaction) followed by dynamic crystallization were achieved without using an external chiral source. Since the DA reaction of 2-methylfuran and various maleimides proceeds reversibly, an exo-adduct was obtained as the main product as the reaction proceeded. From single crystal X-ray structure analysis, it was found that five of ten exo-adducts gave conglomerates. When 2-methylfuran and various maleimides with a catalytic amount of TFA were reacted in a sealed tube, the exo-DA adducts were precipitated from the solution, while the reaction mixtures were continuously ground and stirred using glass beads. Deracemization occurred and chiral amplification was observed for four of the substrates. Each final enantiomeric purity was influenced by the crystal structure, and when enantiomers were included in the disorder, they reached an enantiomeric purity reflecting the ratio of the disorder. The final ee value of the 3,5-dimethylphenyl derivative after chiral amplification was 98% ee.

Keywords: amplification of chirality; dynamic crystallization; Diels–Alder reaction; absolute asymmetric synthesis; conglomerate; racemization; attrition-enhanced deracemization; Viedma ripening; reversible reaction; enantiomorph; crystal; polymorphism

1. Introduction

The Diels–Alder (DA) reaction is one of the most important and fundamental organic synthesis reactions, achieving the concerted [4 + 2] cycloaddition of a diene and an alkene [1,2]. Because it can form two C-C single bonds in one step, it is used to create many cyclic compounds including polycyclic compounds (Figure 1) [3–10]. In addition, a number of asymmetric reactions have been reported, since these can theoretically construct four asymmetric centers at once. Excellent catalytic asymmetric synthesis [11–20] and diastereoselective reactions of chiral substrates have also been reported [21–24]. Each of these reactions is an asymmetric induction method using an enantiomerically active catalyst or substrate and constructs a diastereoselective environment in the transition state of the reaction.

Figure 1. Valuable Diels–Alder reaction constructing numerous cyclic compounds.
In contrast to reactions using chiral sources as starting materials and catalysts, asymmetric synthesis using chirality that occurs naturally when organic compounds crystallize has been reported in recent years (Figure 2) [25]. In this method, a compound having a chiral center is generated from a prochiral substrate, and a dynamic preferential crystallization accompanied by the racemization of the generated chiral center is performed continuously without using any external asymmetric source. It is possible to obtain a crystal of the product having a high enantiomeric purity. The racemization process of the product includes a reaction that regenerates a prochiral starting material via a reverse reaction or a process via a direct racemization reaction of an asymmetric center.

**Figure 2.** Absolute asymmetric synthesis involving dynamic crystallization from prochiral starting materials under achiral conditions.

These synthetic reactions are absolute asymmetric syntheses that provide enantiomerically active compounds from prochiral substrates without using an external chiral source; this is a phenomenon that is of wide interest to researchers in many academic fields [26–30]. Successful absolute asymmetric synthesis by fusion of the reaction that forms the chiral center from prochiral starting materials and the subsequent dynamic crystallization process have been reported in several reaction systems. For example, the Mannich-type reaction [31], aldol reaction [32], stereoisomerization of succinimide [25], synthesis of isoindolinone [33], aza-Michael addition [34–36], Strecker reaction [37,38], and a photochemical reaction [39,40] have all been achieved under achiral conditions. In these limited examples, crystals with high ee were obtained from prochiral materials, and this method is expected to be applied to many reaction systems.

We recently reported the asymmetric Diels–Alder reaction of prochiral starting materials leading to a conglomerate crystal of the adduct in enantiomerically active form [41]. When 2-methylfuran and N-phenylmaleimide were reacted with a small amount of solvent and a catalytic amount of trifluoroacetic acid in a sealed tube at 80 °C, the racemic exo-adduct quickly precipitated. Subsequently, the continuous suspension of the reaction mixture with glass beads promoted the chiral amplification to 90% ee by attrition-enhanced deracemization (Figure 3). In this phenomenon, a racemic product having a chiral center is first formed by a DA reaction from a prochiral substance, followed by preferential crystallization of conglomerate crystals. In the mother liquor, by returning to the prochiral substrate by the reverse reaction (retro-DA reaction), the racemic condition is always maintained, preventing the excessive formation of the enantiomer.

In this asymmetric amplification by dynamic crystallization, attrition-enhanced deracemization was quite effective in promoting Viedam ripening by continuous grinding of the crystals using glass beads, and finally, the enantiomer crystals converged to high enantiomeric purity [42]. This technique was followed in the deracemization reaction from a racemic mixture of NaClO₃ and has recently been
We succeeded in the asymmetric DA reaction utilizing the fact that the DA adduct of 2-methylfuran and pharmaceutical and agricultural chemical intermediates [43–54]. A key feature of this technique is that it can be applied to deracemization in a system with a relatively low racemization rate, as compared with the method of promoting crystallization using a solvent evaporation method or a temperature gradient [55–58].

![Figure 3. Diels–Alder (DA) reaction of 2-methylfuran and N-phenylmaleimide.](image)

The bottleneck of deracemization by the dynamic crystallization method is whether or not the target substrate crystallizes as a stable conglomerate. The occurrence of racemic mixtures crystallizing as a conglomerate is approximately 5–10% [59–62]. However, some substrates form conglomerates or chiral crystals at a very high rate due to the effects of molecular shapes and intermolecular interactions. We succeeded in the asymmetric DA reaction utilizing the fact that the DA adduct of 2-methylfuran and N-phenylmaleimide was a conglomerate [41]. However, to investigate the generality of this methodology, we synthesized and analyzed a variety of DA adducts with various substituents on the nitrogen atom (Figure 4).

![Figure 4. Asymmetric Diels–Alder reaction of 2-methylfuran and various N-arylmaleimides converged to one-handed enantiomorphic crystals.](image)

Analysis of the crystal structures of the adducts revealed that they exhibited a very high probability of affording conglomerates. For these substrates, we achieved an asymmetric DA reaction without using an external chiral source and clarified the relationship between the crystal structure and the enantiomeric purity of the products.

2. Results and Discussion

In order to investigate the effect of the substituent on the nitrogen atom of the DA adduct on the crystal structure and the enantiomeric purity of the crystal in dynamic crystallization, the adducts exo-3b–j were synthesized by changing the substituent as shown in Table 1.
Table 1. Space groups of exo-3.

| exo-3   | R            | Space Group          |
|---------|--------------|----------------------|
| 3a      | C₆H₅        | P₂₁ 2₁ 2₁ [a]        |
| 3b      | 4-ClC₆H₄    | P₂₁ 2₁ 2₁, (73:27)   |
| 3c      | 3,4-Me₂C₆H₃| P₂₁ 2₁ 2₁            |
| 3d      | 3,5-ClC₆H₃ | P₂₁, (76:24) [b]     |
| 3e      | 4-MeC₆H₄   | P₂₁ 2₁ 2₁, polymorphism [c] |
| 3f      | 4-FC₆H₄    | P₂₁/c                |
| 3g      | 4-BrC₆H₄   | P₂₁/n                |
| 3h      | 3-MeC₆H₄   | ND [d]               |
| 3i      | 4-EtC₆H₄   | ND [d]               |
| 3j      | 4-MeOC₆H₄  | ND [d]               |

[a] Reference No. 41. [b] Disordered crystal consisting of the ratio of both enantiomers indicated in parentheses. [c] Determined by PXRD. [d] Not determined; however, SHG property was inactive by 1064 nm line from an Nd-YAG pulsed laser.

In the DA reaction between 2-methylfuran 1 and maleimides 2b–j, the formation of endo-isomers was confirmed at the beginning of the reaction as in the case of the reaction with 2a [41]. When the reaction time was extended, the products predominantly converged to exo-isomers, because the crystalline exo-adducts were excluded from the reaction system in solution. Therefore, the crystals of the exo-adducts were analyzed by single crystal X-ray structure analysis. When the racemate of each exo-isomer was recrystallized, single crystals suitable for crystal structure analysis were obtained for exo-3b–g. The crystal space groups of these seven types of crystals are shown in Table 1. All of them had 2₁ helices in the crystal lattices. The space group of 3a–3c and 3e was the orthorhombic P₂₁ 2₁ 2₁, and 3d and 3f–g were in the monoclinic space group. Surprisingly, five of the ten synthesized substrates, 3a–3e, formed conglomerates of a chiral crystal space group.

In all cases, interactions such as CH–π, C=O–HC and O–HC with relatively small energies were present, which controlled the molecular arrangement (Figures S1–S8). These molecules had nearly spherical shapes and were closely packed in the crystal. Even when alcohol or benzene-based solvents were used, solvent molecules were not incorporated into the crystals.

For 3h–j, single crystals suitable for X-ray crystallography could not be obtained, thus the detailed molecular arrangements were unknown. However, the second harmonic generation (SHG) of these crystals was inactive by irradiation with 1064 nm light from an Nd-YAG pulsed laser, indicating that they might be racemic crystals [63,64]. However, if the emission of the SHG is weak, the possibility of a conglomerate may have been overlooked.

For asymmetric synthesis by the proposed method, the product crystals must be conglomerates. For the four new substrates 3b–3e determined to be in a chiral crystal space group from the above crystal structure analysis, we investigated the absolute asymmetric DA reaction via asymmetric amplification by crystallization.

Another requisite for chiral amplification by dynamic crystallization is rapid racemization under crystallization conditions. Adducts 3 have four chiral centers determined uniquely in the one-step concerted reaction and these cannot directly racemize. However, apparent racemization occurs due to the equilibrium reaction with a reverse DA reaction to regenerate achiral furan and maleimide [65] (Figure 5).

Utilizing this reversible DA reaction, a deracemization reaction by dynamic crystallization was developed. Many dynamic crystallization methods require rapid racemization under crystallization conditions. However, attrition-enhanced deracemization, which is a method based on crystal grinding, has been reported in many successful cases even in systems with a low racemization rate compared to dynamic preferential crystallization methods using a temperature gradient or solvent evaporation [55–58]. However, fast deracemization under the racemization conditions suppresses side reactions, and crystals with high enantiomeric purity can be obtained efficiently.
Figure 5. Asymmetric synthesis of Diels–Alder reaction products involving racemization via reversible reaction and preferential crystallization.

In the case of the asymmetric synthesis of \textit{exo-3a}, we already found out that trifluoroacetic acid (TFA) was the best catalyst for both of the forward and reverse reactions. NMR spectroscopy was used to follow the reversible reaction at 60 °C in deuterated chloroform. Even when the substituents were changed, the catalytic activity of TFA was effective, and the reaction rate was improved in both the DA and \textit{retro-DA} reversible reactions without side reactions. Table 2 shows the half-life of each substrate. For \textit{1a}, as reported in a previous paper, the addition reaction of maleimide reached 50\% in about 1 h (Table 2), and an \textit{endo}-adduct was formed at the initial stage of the reaction, which eventually converged to an \textit{exo}-adduct over time [41]. In other cases, almost the same courses in the reactions were observed (Figures S9–S11). The change with time, in these cases, is a reaction in a homogeneous system, but the actual reaction is performed at a higher concentration, where the highly crystalline \textit{exo}-adduct is crystallized and removed from the reaction system.

Table 2. The half-life of DA and \textit{retro-DA} reactions with or without trifluoroacetic acid (TFA) [a].

| Substrate | \(\tau_{1/2}\) of DA (2 h) | \(\tau_{1/2}\) of \textit{exo-3} (h) |
|-----------|-----------------|-----------------|
| \(\text{DA w/o TFA} [b]\) | \(\text{DA with TFA} [c]\) | \(\text{retro-DA w/o TFA} [d]\) | \(\text{retro-DA with TFA} [e]\) |
| a [f]    | 0.92            | 0.25            | 4.5         | 3.0         |
| b        | 0.30            | <0.1            | 4.0         | 2.0         |
| c        | 0.42            | <0.1            | 6.5         | 3.2         |
| d        | 0.30            | <0.1            | 2.0         | 1.2         |

[a] All reactions were monitored by \(1^H\) NMR spectroscopy. [b] Conditions: maleimide (0.05 M) and 2-methylfuran (0.5 M) in CDCl\(_3\) at 60 °C. [c] Conditions: maleimide (0.05 M), 2-methylfuran (0.5 M), and TFA (0.05 M) in CDCl\(_3\) at 60 °C. [d] Conditions: \textit{exo-3} (0.05 M) in CDCl\(_3\) at 60 °C. [e] Conditions: \textit{exo-3} (0.03 M) and TFA (0.03 M) in CDCl\(_3\) at 60 °C. [f] Reference No. 41.

The reaction in the NMR tube was also examined for the reverse reaction. The degradation of \textit{exo-3} at low concentration (0.05 M) in deuterated chloroform at 60 °C was followed. Maleimide 2 and methylfuran 1 were quantitatively regenerated in all cases. In order to perform highly efficient...
deracemization, it was necessary to accelerate both the forward and reverse reactions. Specifically, it was necessary to search for a catalyst that greatly accelerated the reverse reaction.

When various maleimides 2a–d were reacted with 2-methylfuran in the presence of TFA, the DA reaction was accelerated about 4 times for most substrates. Regarding the reverse reaction, it was found that when exo-3a–d were reacted with TFA in the same concentration of 0.03 M, the reaction was accelerated by 1.5 to 2 times compared to the reaction without TFA (Table 2, Figures S9–S11). Table 2 shows the results at 60 °C, but the actual reaction can be run at 80 °C, whereupon the rate is expected to be several times faster, and a sufficient reversible reaction rate is ensured.

Once the formation of conglomerates and the progress of racemization were confirmed, the asymmetric synthesis involving the dynamic crystallization process was examined. In a sealed tube, N-arylmaleimide 2 (100 mg), 2-methylfuran 1 (15.0 equiv), TFA (0–1.0 equiv) as the catalyst, heptane (1.0 mL) as a solvent, and glass beads (2 mmØ, 250 mg) were added to crush the crystals and the mixture was stirred at 80 °C for several days. The DA reaction proceeded immediately after the start of the reaction, and within a few minutes, crystals of the adducts precipitated and the reaction solution was suspended. After that, deracemization occurred by continuously stirring the obtained suspension. The change in ee value of exo-3 by deracemization was monitored by HPLC using a CHIRALPAK IA (Daicel Ind.) column.

In our previous paper, when 0.5 equiv of TFA was used, the enantiomeric purity started to increase after six days from the start of the reaction and reached 90% ee after 14 days (Figure 6) [41]. Thereafter, the suspension was filtered to isolate the crystals, and exo-3a was obtained with a yield of 80% and 90% ee. The plot of enantiomeric purity versus time showed a non-linear curve. This sigmoid-like increase in enantiomeric purity is typical for Viedma ripening, and the population balance model [66,67] and existing formulas were extended in view of the effects of Ostwald ripening and autocatalytic enantioselective crystal growth. Theoretical analysis by fitting [68,69] has also been performed. On the other hand, when no glass beads were used, deracemization did not occur.

Based on the results of the asymmetric reaction of 2a to exo-3a, asymmetric DA reactions for 2b–2e with 1 were also examined leading to conglomerates exo-3b–3e. As in the case of the reaction of 2a, 2-methylfuran 1, various N-arylmaleimides 2b–2e, 0.5 equiv of TFA as a catalyst for promoting racemization, heptane as a solvent, and glass beads for grinding the precipitated solids were stirred in a sealed tube at 80 °C for several days while tracking the change of the ee value of the solid exo-3 (Table 3 and Figure 6).
Table 3. Asymmetric DA reaction of 3a-d [a].

|   | Time (day) [b] | Yield (%) [c] | Ee (%) [d] |
|---|---------------|---------------|------------|
| 3a | 6-14          | 80            | 90         |
| 3b | 7-15          | 70            | 40         |
| 3c | 3-9           | 81            | 98         |
| 3d | 4-8           | 78            | 49         |

[a] Conditions: prochiral 2 (100 mg), 2-methylfuran 1 (5.0 equiv), TFA (0.5 equiv), heptane (1.00 mL), and glass beads (250 mg) were stirred at 80 °C in a sealed tube. [b] Time required for asymmetric expression and amplification. [c] Yields of crystalline 3 after filtration. [d] Enantiomeric excess of crystals of 3. [e] Reference No. 41.

When 2b was used, crystals of DA adduct were precipitated immediately after the reaction, and the continuous stirring while suspending the solids led to an increase in the enantiomeric purity of exo-3b from the 7th day, reaching 40% ee after 15 days. However, no further asymmetric amplification occurred. This is attributable to the crystal structure of exo-3b. Disordered packing was indicated by single-crystal structure analysis, and the ratio of the enantiomers was 73:27, a result that exactly reflected the ee value of the converged enantiomorphic crystals.

In the case of 2c, the crystallinity of the produced exo-3c was also good, and a stable suspension by glass beads and the stir bar was obtained. The ee value of exo-3c increased after 3 days and reached 98% after 9 days, achieving the most efficient asymmetric amplification among all the substrates.

When 2d was used, immediately after the reaction, crystals were precipitated, a suspension was obtained, and asymmetric amplification started 4 days later. Eight days later, the ee reached 49%, after which further amplification did not occur. The reason for this limitation is that, similar to the case of exo-3b, due to the crystal packing of exo-3d, the enantiomer contained in the single crystal is disordered in a ratio of 74:26, which exactly reflected the maximum ee value of exo-3d.

The asymmetric synthesis of exo-3e using maleimide 2e was also examined, but exo-3e was obtained as a racemate without asymmetric amplification. The powdered X-ray crystal structure analysis of the obtained solid was different from the analysis pattern simulated from the conglomerate crystal P212121 (Figure 7). Conglomerate crystals of exo-3e gradually changed to a racemic crystal system during suspension with glass beads. The crystal does not contain a crystallization solvent and it showed a polymorphism with a phase transition.

![Figure 7. PXRD pattern of exo-3e: (a) powder of exo-3e after grinding, (b) calculated pattern from a single crystal of exo-3e of the P212121 space group.](image)

It was unable to control the handedness of the crystals obtained after the DA reaction; solids of both types of handedness were obtained in approximately the same number of times for every ten experiments. However, we were able to control the handedness by starting the attrition-enhanced...
deracemization from a DA adduct with low ee (5% ee). The deracemization started immediately and the same handedness of the enantiomer as the slightly excess stereoisomer could be efficiently obtained.

3. Conclusions

Asymmetric DA reactions from prochiral starting materials involving dynamic preferential crystallization were achieved under achiral conditions. Since the DA reaction of 2-methylfuran and various maleimide derivatives proceeded reversibly, exo-adducts were obtained as major products as the reaction proceeded. Nine exo-adducts were newly synthesized by the DA reaction using maleimides with various substituents on the nitrogen atom. Single crystal X-ray structure analysis revealed that four derivatives gave conglomerates.

When 2-methylfuran and each maleimide in the presence of a catalytic amount of TFA were reacted in a sealed tube, DA adducts precipitated as crystals. The mixture was continuously ground and stirred using glass beads. Deracemization of exo-type DA adducts occurred and asymmetric amplification was observed for four substrates. Each final enantiomeric purity was greatly influenced by the crystal structure, and when enantiomers were included in the disorder, they reached an enantiomeric purity reflecting the ratio. In addition, it was found that the chirality of the 3,5-dimethylphenyl derivative was deracemized to 98% ee. We have developed an absolute asymmetric DA reaction that can obtain enantiomerically active DA adducts without using an external asymmetric source.

4. Experimental

General Information. NMR spectra were recorded in CDCl$_3$ solutions on a Bruker DPX 300 and DPX 400 spectrometers for $^1$H- and $^{13}$C-NMR. Chemical shifts are reported in parts per million (ppm) relative to TMS as an internal standard. IR spectra were recorded on a JASCO FT/IR-230 spectrometer. HPLC analyses were performed on a JASCO HPLC system (JASCO PU-1580 pump, DG-1580-53, LG-2080-02, MD-2015, UV-2075 and CD-2095 detector). Single crystal X-ray structure analysis was conducted using a SMART APEX II (Bruker AXS) and APEX II ULTRA (Bruker AXS). Powder X-ray crystallographic analysis was performed using D8 ADVANCE (BRUKER AXS). Commercially available N-phenylmaleimide and 2-methylfuran were used without further purification. Other maleimides 2b–j were provided according to the reported procedure [70,71]. (Figures S18–S35)

Synthesis of Exo-3a–j.

The corresponding maleimides 2 (1.0 g) and 2-methylfuran 1 (15 equiv) were added to 10 mL of hexane, and the mixture was stirred at 60 °C for 24 h. Thereafter, the solvent and extra amount of methylfuran were removed under reduced pressure, and the crude crystalline products were recrystallized from chloroform/hexane to isolate exo-3. The structures of known adducts 3a were determined by comparing their spectral data to literature values. The adducts, 3e–g, and 3j are commercially available; however, these materials were easily obtained by the above method.

(3aS*,4R*,7S*,7aR*)-4-Methyl-2-phenyl-3a,4,7,7a-tetrahydro-1$^H$-4,7-epoxyisoindole-1,3(2$^H$)-dione (exo-3a) [41]

Colorless prism; 96% yield; mp: 144–146 °C; $^1$H NMR (CDCl$_3$) δ 1.80 (s, 3H), 2.88 (d, J = 6.6 Hz, 1H), 3.14 (d, J = 6.3 Hz, 1H), 5.32 (d, J = 1.5 Hz, 1H), 6.38 (d, J = 5.7 Hz, 1H), 6.57 (dd, J = 1.5 and 5.4 Hz, 1H), 7.27–7.30 (m, 2H), 7.37–7.51 (m,3H); $^{13}$C NMR (CDCl$_3$) δ 15.7, 49.5, 50.6, 81.1, 88.6, 126.5, 128.7, 129.1, 131.7, 137.1, 140.7, 174.0, 175.3. (Figures S36 and S37) The enantiomeric purity of the solid was determined by HPLC using a CHIRALPAK IA (Daicel Ind.); column. $t_R(1) = 20$ min for (+)-3a, $t_R(2) = 30.5$ min for (−)-3a. Eluent: hexane/EtOH = 80:20 (v/v); flow rate: 0.7 mL/min.

(3aS*,4R*,7S*,7aR*)-2-(4-Chlorophenyl)-4-methyl-3a,4,7,7a-tetrahydro-1H-4,7-epoxyisoindole-1,3(2$^H$)-dione (exo-3b)

Colorless crystal; m.p. 120 °C; 90% yield; $^1$H NMR (CDCl$_3$) δ 1.78 (s, 3H), 2.85 (d, J = 6.5 Hz, 1H), 3.11 (d, J = 6.5 Hz, 1H), 5.29 (d, J = 1.8 Hz, 1H), 6.37 (d, J = 5.6 Hz, 1H), 6.55 (dd, J = 5.6, 1.6 Hz, 1H), 7.23–7.26 (m, 2H), 7.42–7.44 (m, 2H); $^{13}$C NMR (CDCl$_3$) δ 15.7, 49.5, 50.6, 81.1, 88.6, 127.7, 129.2, 130.2,
134.4, 137.0, 140.7, 173.7, 175.0; IR (cm⁻¹, KBr) 1701; HRMS (ESI-MS) m/z calcd for C₁₃H₁₂CINO₃ + H 290.0578, found 290.0577. (Figures S38 and S39) The enantiomeric purity of the solid was determined by HPLC using a CHIRALPAK IA (Daicel Ind.); column. $t_{R(1)} = 20$ min for (+)-3b, $t_{R(2)} = 22$ min for (−)-3b. Eluent: hexane/EtOH = 90: 10 (v/v); flow rate: 1.0 mL/min. (Figures S12 and S13)

(3aS*,4R*,7S*,7aR*)-2-(3,4-Dimethylphenyl)-4-methyl-3a,4,7,7a-tetrahydro-1H-4,7-epoxyisoindole-1,3 (2H)-dione (exo-3c)

Colorless crystal; m.p. 140 °C; 91% yield; ¹H NMR (CDCl₃) δ 1.78 (s, 3H), 2.27 (s, 3H), 2.27 (s, 3H), 2.84 (d, J = 6.5 Hz, 1H), 3.10 (d, J = 6.5 Hz, 1H), 5.30 (d, J = 1.6 Hz, 1H), 6.36 (d, J = 5.6 Hz, 1H), 6.54 (dd, J = 5.6, 1.6 Hz, 1H), 6.96–7.01 (m, 2H), 7.21–7.26 (m, 1H); ¹³C NMR (CDCl₃) δ 15.7, 19.5, 19.8, 49.4, 50.6, 81.0, 88.5, 123.9, 127.5, 129.2, 130.2, 137.0, 137.6, 140.7, 174.2, 175.6; IR (cm⁻¹, KBr) 1708; HRMS (ESI-MS) m/z calcd for C₁₇H₁₇NO₃ + H 284.1281, found 284.1276. (Figures S40 and S41) The enantiomeric purity of the solid was determined by HPLC using a CHIRALPAK IA (Daicel Ind.); column. $t_{R(1)} = 29.5$ min for (+)-3c, $t_{R(2)} = 33$ min for (−)-3c. Eluent: hexane/EtOH = 80: 20 (v/v); flow rate: 0.5 mL/min. (Figures S14 and S15)

(3aS*,4R*,7S*,7aR*)-2-(3,5-Dichlorophenyl)-4-methyl-3a,4,7,7a-tetrahydro-1H-4,7-epoxyisoindole-1,3 (2H)-dione (exo-3d)

Colorless crystal; m.p. 136 °C; 99% yield; ¹H NMR (CDCl₃) δ 1.79 (s, 3H), 2.87 (d, J = 6.5 Hz, 1H), 3.13 (d, J = 6.5 Hz, 1H), 5.30 (d, J = 1.8 Hz, 1H), 6.38 (d, J = 5.6 Hz, 1H), 6.57 (dd, J = 5.6, 1.6 Hz, 1H), 7.26 (2H), 7.39–7.40 (m, 1H); ¹³C NMR (CDCl₃) δ 15.7, 49.5, 50.6, 81.2, 88.7, 125.1, 128.8, 133.3, 135.2, 140.7, 173.2, 174.5; IR (cm⁻¹, KBr) 1712. (Figures S42 and S43) The enantiomeric purity of the solid was determined by HPLC using a CHIRALPAK IA (Daicel Ind.); column. $t_{R(1)} = 13.5$ min for (+)-3d, $t_{R(2)} = 16$ min for (−)-3d. Eluent: hexane/EtOH = 90 : 10 (v/v); flow rate: 1.0 mL/min. (Figures S16 and S17)

(3aS*,4R*,7S*,7aR*)-4-Methyl-2-(4-tolyl)-3a,4,7,7a-tetrahydro-1H-4,7-epoxyisoindole-1,3(2H)-dione (exo-3e)

Colorless crystal; m.p. 132 °C; 90% yield; ¹H NMR (CDCl₃) δ 1.79 (s, 3H), 2.38 (s, 3H), 2.86 (d, J = 6.6 Hz, 1H), 3.12 (d, J = 6.6 Hz, 1H), 5.31 (d, J = 1.8 Hz, 1H), 6.37 (d, J = 5.5 Hz, 1H), 6.56 (dd, J = 5.6, 1.7 Hz, 1H), 7.13–7.28 (m, 4H); ¹³C NMR (CDCl₃) δ 15.7, 21.2, 49.4, 50.6, 81.0, 88.5, 126.3, 129.1, 129.7, 137.0, 138.7, 140.7, 174.1, 175.4; IR (cm⁻¹, KBr) 1707. (Figures S44 and S45)

(3aS*,4R*,7S*,7aR*)-2-(4-Fluorophenyl)-4-methyl-3a,4,7,7a-tetrahydro-1H-4,7-epoxyisoindole-1,3(2H)-dione (exo-3f)

Colorless crystal; m.p. 133 °C; 88% yield; ¹H NMR (CDCl₃) δ 1.78 (s, 3H), 2.86 (d, J = 6.5 Hz, 1H), 3.11 (d, J = 6.5 Hz, 1H), 5.29 (d, J = 1.8 Hz, 1H), 6.37 (d, J = 5.6 Hz, 1H), 6.55 (dd, J = 5.7, 1.7 Hz, 1H), 7.13–7.29 (m, 4H); ¹³C NMR (CDCl₃) δ 15.7, 49.4, 50.6, 81.1, 88.6, 116.0, 116.2, 127.6, 128.3, 128.4, 137.0, 140.7, 160.9, 163.4, 173.9, 175.2. (Figures S46 and S47)

(3aS*,4R*,7S*,7aR*)-2-(4-Bromophenyl)-4-methyl-3a,4,7,7a-tetrahydro-1H-4,7-epoxyisoindole-1,3(2H)-dione (exo-3g)

Colorless crystal; m.p. 127 °C; 94% yield; ¹H NMR (CDCl₃) δ 1.78 (s, 3H), 2.86 (d, J = 6.5 Hz, 1H), 3.12 (d, J = 6.5 Hz, 1H), 5.29 (d, J = 1.8 Hz, 1H), 6.37 (d, J = 5.6 Hz, 1H), 6.56 (dd, J = 5.7, 1.7 Hz, 1H), 7.18–7.20 (m, 2H), 7.58–7.60 (m, 2H); ¹³C NMR (CDCl₃) δ 15.7, 49.5, 50.6, 81.1, 88.6, 122.5, 128.0, 130.6, 132.2, 137.0, 140.7, 173.6, 174.9; IR (cm⁻¹, KBr) 1705. (Figures S48 and S49)

(3aS*,4R*,7S*,7aR*)-4-Methyl-2-(3-tolyl)-3a,4,7,7a-tetrahydro-1H-4,7-epoxyisoindole-1,3(2H)-dione (exo-3h)

Colorless crystal; m.p. 128 °C; 93% yield; ¹H NMR (CDCl₃) δ 1.79 (s, 3H), 2.38 (s, 3H), 2.86 (d, J = 6.5 Hz, 1H), 3.12 (d, J = 6.5 Hz, 1H), 5.31 (d, J = 1.6 Hz, 1H), 6.37 (d, J = 5.6 Hz, 1H), 6.55 (dd, J = 5.6, 1.6 Hz, 1H), 7.05–7.37 (m, 4H); ¹³C NMR (CDCl₃) δ 15.7, 21.3, 49.5, 50.6, 81.1, 88.6, 123.6, 127.1, 128.9, 129.6, 131.6, 137.0, 139.2, 140.7, 174.1, 175.4; IR (cm⁻¹, KBr) 1707; HRMS (ESI-MS) m/z calcd for C₁₆H₁₅NO₃ - H 268.0979, found 288.0992. (Figures S50 and S51)
(3aS*,4R*,7S*,7aR*)-2-(4-Ethylphenyl)-4-methyl-3a,4,7,7a-tetrahydro-1H-4,7-epoxyisoindole-1,3(2H)-dione (exo-3i)

Colorless crystal; m.p. 114 °C; 88% yield; 1H NMR (CDCl₃) δ 1.24 (t, J = 7.7 Hz, 3H), 1.79 (s, 3H), 2.67 (q, J = 7.6 Hz, 2H), 2.85 (d, J = 6.5 Hz, 1H), 3.11 (d, J = 6.5 Hz, 1H), 5.30 (d, J = 1.8 Hz, 1H), 6.36 (d, J = 6.5 Hz, 1H), 6.55 (dd, J = 5.6, 1.6 Hz, 1H), 7.16-7.30 (m, 4H), 13C NMR (CDCl₃) δ 15.3, 15.7, 28.6, 49.5, 50.6, 81.1, 88.6, 126.4, 128.6, 129.3, 137.0, 140.7, 144.9, 174.2, 175.5; IR (cm⁻¹) KBr 1702; HRMS (ESI-MS) m/z calcd for C₁₇H₁₇N₂O₃ + H 284.1271, found 284.1277. (Figures S52 and S53)

(3aS*,4R*,7S*,7aR*)-2-(4-Methoxyphenyl)-4-methyl-3a,4,7,7a-tetrahydro-1H-4,7-epoxyisoindole-1,3(2H)-dione (exo-3j)

Colorless crystal; m.p. 120–121 °C; 94% yield; 1H NMR (CDCl₃) δ 1.78 (s, 3H), 2.84 (d, J = 6.5 Hz, 1H), 3.10 (d, J = 6.5 Hz, 1H), 3.82 (s, 3H), 5.29 (d, J = 1.8 Hz, 1H), 6.36 (d, J = 5.7 Hz, 1H), 6.54 (dd, J = 5.6, 1.6 Hz, 1H), 6.94–7.26 (m, 4H), 13C NMR (CDCl₃) δ 15.7, 49.4, 50.5, 55.4, 81.0, 88.5, 114.4, 124.4, 127.7, 137.0, 140.7, 159.5, 174.3, 175.5. (Figures S54 and S55)

Single crystal X-ray structure analysis of (3aS,4R,7S,7aR)-2-(4-chlorophenyl)-4-methyl-3a,4,7,7a-tetrahydro-1H-4,7-epoxyisoindole-1,3(2H)-dione (exo-3b)

Disordered crystal of the ratio of 73:27, exhibiting (-)-CD sign at 254 nm for major isomer. Colorless prism (0.20 × 0.20 × 0.01 mm³), orthorhombic space group P₂₁₂₁, a = 6.5485(4) Å, b = 12.3747(6) Å, c = 16.8764(9) Å, V = 1363.24(8) Å³, Z = 4, λ (CuKα) = 1.54178 Å, ρ = 1.407 g/cm³, μ (CuKα) = 2.539 cm, 3954 reflections measured (T = 173 K, 4.430° < θ < 68.264°), nb of independent data collected: 2213 nb of independent data used for refinement: 2127 in the final least-squares refinement cycles on F², the model converged at R₁ = 0.0505, wR₂ = 0.1993 [I > 2σ(I)], R₁ = 0.0522, wR₂ = 0.1408 (all data), and GOF = 1.065, H-atom parameters constrained, absolute Flack parameter = 0.505(8). (CCDC 1985809). (Figure S1)

Single crystal X-ray structure analysis of (3aS,4R,7S,7aR)-2-(3,4-dimethylphenyl)-4-methyl-3a,4,7,7a-tetrahydro-1H-4,7-epoxyisoindole-1,3(2H)-dione (exo-3c)

Enantiomerically pure crystal provided by optical resolution using HPLC, exhibiting (-)-CD sign at 254 nm. Colorless prism (0.20 × 0.20 × 0.01 mm³), orthorhombic space group P₂₁₂₁, a = 6.5975(2) Å, b = 12.3565(4) Å, c = 16.7223(6) Å, V = 1363.24(8) Å³, Z = 4, λ (CuKα) = 1.54178 Å, ρ = 1.412 g/cm³, μ (CuKα) = 2.547 cm, 12970 reflections measured (T = 173 K, 4.430° < θ < 68.213°), nb of independent data collected: 2427, nb of independent data used for refinement: 2397 in the final least-squares refinement cycles on F², the model converged at R₁ = 0.0369, wR₂ = 0.0985 [I > 2σ(I)], R₁ = 0.0371, wR₂ = 0.0989 (all data), and GOF = 1.059, H-atom parameters constrained, absolute Flack parameter = 0.051(3). (CCDC 1985810). (Figure S2)

Single crystal X-ray structure analysis of (3aS,4R,7S,7aR)-2-(3,5-dichlorophenyl)-4-methyl-3a,4,7,7a-tetrahydro-1H-4,7-epoxyisoindole-1,3(2H)-dione (exo-3d)

Exhibiting (-)-CD sign at 254 nm. Colorless prism (0.20 × 0.20 × 0.01 mm³), orthorhombic space group P₂₁₂₁, a = 7.9707(3) Å, b = 12.9386(5) Å, c = 13.7305(5) Å, V = 1416.02(9) Å³, Z = 4, λ(CuKα) = 1.54178 Å, ρ = 1.329 g/cm³, μ(CuKα) = 0.741 cm, 21885 reflections measured (T = 173 K, 4.696° < θ < 68.241°), nb of independent data collected: 2593, nb of independent data used for refinement: 2576 in the final least-squares refinement cycles on F², the model converged at R₁ = 0.0334, wR₂ = 0.0855 [I > 2σ(I)], R₁ = 0.0335, wR₂ = 0.0856 (all data), and GOF = 1.065, H-atom parameters constrained, absolute Flack parameter = 0.099(16). (CCDC 1985811). (Figure S3)

Single crystal X-ray structure analysis of (3aS,4R,7S,7aR)-2-(3,5-dichlorophenyl)-4-methyl-3a,4,7,7a-tetrahydro-1H-4,7-epoxyisoindole-1,3(2H)-dione (exo-3e)

Disordered crystal of the ratio of 76:24, exhibiting (-)-CD sign at 254 nm for major isomer. Colorless prism (0.30 × 0.20 × 0.20 mm³), monoclinic space group P₂₁, a = 5.4032(5) Å, b = 13.9697(10) Å, c = 9.6673(8) Å, β = 105.179(4)°, V = 704.24(10) Å³, Z = 2, λ(CuKα) = 1.54178 Å, ρ = 1.529 g/cm³, μ(CuKα) = 4.237 cm, 2350 reflections measured (T = 173 K, 5.7024° < θ < 68.068°), nb of independent data collected: 1457, nb of independent data used for refinement: 1452 in the final least-squares refinement
cycles on $F^2$, the model converged at $R_1 = 0.0532$, $wR_2 = 0.1391$ [$I > 2\sigma(I)$], $R_1 = 0.0532$, $wR_2 = 0.1392$ (all data), and GOF = 1.125, H-atom parameters constrained, absolute Flack parameter = 0.12(3). (CCDC 1985812). (Figure S4)

Single crystal X-ray structure analysis of (3aR,4S,7R,7aS)-2-(3,5-dichlorophenyl)-4-methyl-3a,4,7,7a-tetrahydro-1H-4,7-epoxyisoindole-1,3(2H)-dione (exo-+)-3d

Enantiomerically pure crystal provided by optical resolution using HPLC. Colorless prism (0.30 × 0.20 × 0.20 mm$^3$), monoclinic space group $P2_1$, $a = 5.3713(9)$ Å, $b = 13.958(2)$ Å, $c = 9.5751(14)$ Å, $\beta = 103.609(5)^\circ$, $V = 697.72(19)$ Å$^3$, $Z = 2$, $\lambda(CuK\alpha) = 1.54178$ Å, $\rho = 1.316$ g/cm$^3$, $\mu(CuK\alpha) = 4.277$ cm$^{-1}$, 10993 reflections measured ($T = 173$ K, 4.752$^\circ$ < $\theta$ < 72.198$^\circ$), nb of independent data collected: 2558, nb of independent data used for refinement: 2225 in the final least-squares refinement cycles on $F^2$, the model converged at $R_1 = 0.0429$, $wR_2 = 0.1034$ [$I > 2\sigma(I)$], $R_1 = 0.0431$, $wR_2 = 0.1036$ (all data), and GOF = 1.101, H-atom parameters constrained, absolute Flack parameter = 0.110(5). (CCDC 1985813). (Figure S5)

Single crystal X-ray structure analysis of analysis of (3aR,4S,7R,7aS)-4-methyl-2-(4-tolyl)-3a,4,7,7a-tetrahydro-1H-4,7-epoxyisoindole-1,3(2H)-dione (exo-3e)

Colorless prism (0.20 × 0.10 × 0.10 mm$^3$), orthorhombic space group $P2_12_12_1$, $a = 9.3007(6)$ Å, $b = 10.6635(6)$ Å, $c = 13.7010(9)$ Å, $V = 1358.84(15)$ Å$^3$, $Z = 4$, $\lambda(CuK\alpha) = 1.54178$ Å, $\rho = 1.316$ g/cm$^3$, $\mu(CuK\alpha) = 0.746$ cm, 4911 reflections measured ($T = 173$ K, 6.314$^\circ$ < $\theta$ < 68.278$^\circ$), nb of independent data collected: 2263, nb of independent data used for refinement: 2225 in the final least-squares refinement cycles on $F^2$, the model converged at $R_1 = 0.0458$, $wR_2 = 0.1278$ [$I > 2\sigma(I)$], $R_1 = 0.0462$, $wR_2 = 0.1284$ (all data), and GOF = 1.048, H-atom parameters constrained, absolute Flack parameter = 0.39(7). (CCDC 1985814). (Figure S6)

Single crystal X-ray structure analysis of analysis of (3aS*,4R*,7S*,7aR*)-2-(4-fluorophenyl)-4-methyl-3a,4,7,7a-tetrahydro-1H-4,7-epoxyisoindole-1,3(2H)-dione (exo-3f)

Colorless prism (0.20 × 0.10 × 0.03 mm$^3$), monoclinic space group $P2_1/c$, $a = 9.9813(13)$ Å, $b = 13.0236(15)$ Å, $c = 9.7580(8)$ Å, $\beta = 101.379(9)^\circ$, $V = 1243.5(2)$ Å$^3$, $Z = 4$, $\lambda(CuK\alpha) = 1.54178$ Å, $\rho = 1.460$ g/cm$^3$, $\mu(CuK\alpha) = 0.945$ cm, 2238 reflections measured ($T = 173$ K, 5.655$^\circ$ < $\theta$ < 68.328$^\circ$), nb of independent data collected: 2238, nb of independent data used for refinement: 1687 in the final least-squares refinement cycles on $F^2$, the model converged at $R_1 = 0.0687$, $wR_2 = 0.1787$ [$I > 2\sigma(I)$], $R_1 = 0.0915$, $wR_2 = 0.1875$ (all data), and GOF = 1.172, H-atom parameters constrained. (CCDC 1985815). (Figure S7)

Single crystal X-ray structure analysis of (3aS*,4R*,7S*,7aR*)-2-(4-bromophenyl)-4-methyl-3a,4,7,7a-tetrahydro-1H-4,7-epoxyisoindole-1,3(2H)-dione (exo-3g)

Colorless prism (0.20 × 0.20 × 0.20 mm$^3$), monoclinic space group $P2_1/n$, $a = 20.883(6)$ Å, $b = 6.485(2)$ Å, $c = 20.853(6)$ Å, $\beta = 104.364(3)^\circ$, $V = 2729.9(15)$ Å$^3$, $Z = 8$, $\lambda(MoK\alpha) = 0.71073$ Å, $\rho = 1.626$ g/cm$^3$, $\mu(MoK\alpha) = 3.018$ cm, 5224 reflections measured ($T = 173$ K, 1.593$^\circ$ < $\theta$ < 27.570$^\circ$), nb of independent data collected: 5224, nb of independent data used for refinement: 3679 in the final least-squares refinement cycles on $F^2$, the model converged at $R_1 = 0.0511$, $wR_2 = 0.1118$ [$I > 2\sigma(I)$], $R_1 = 0.0928$, $wR_2 = 0.1310$ (all data), and GOF = 1.025, H-atom parameters constrained. (CCDC 1985818). (Figure S8)

Reaction conditions for asymmetric DA reaction via dynamic crystallization

In a sealed tube ($L = 200$ mm, $\Phi = 25$ mm), N-arylmaleimide 2 (100 mg), 2-methylfuran 1 (15 eq.), TFA (0–1.0 eq.), and heptane (1.0 mL) were stirred with or without glass beads (250 mg) using a stir bar at 80 °C. The crystalline adduct 3 appeared after a few minutes, and the solution was kept in suspension by stirring at 600 rpm for several days at 80 °C. The change of ee value of crystalline 3 was monitored by HPLC using CHIRALPAK IA (Daicel Ind.) column; eluent: n-hexane/EtOH. Finally, crystalline exo-3 was isolated by filtration. The same procedure was performed for all substrates.
Supplementary Materials: The following are available online at http://www.mdpi.com/2073-8994/12/6/910/s1,
Figure S1: Single crystal X-Ray crystallographic analysis of exo-3b (disordered), Figure S2: Single crystal
X-Ray crystallographic analysis of exo-3b (enantiopure), Figure S3: Single crystal X-Ray crystallographic
analysis of exo-3e (enantiopure), Figure S4: Single crystal X-Ray crystallographic analysis of exo-3d (disordered),
Figure S5: Single crystal X-Ray crystallographic analysis of exo-3d (enantiopure), Figure S6: Single crystal X-Ray
crystallographic analysis of exo-3f, Figure S7: Single crystal X-Ray crystallographic analysis of exo-3f, Figure S8:
Single crystal X-Ray crystallographic analysis of exo-3g, Figure S9: Time course for DA reaction of 1 (0.5 M) and
2b–d (0.05 M) at 60 °C in CDCl3 monitored by 1H NMR, Figure S10: Time course for reverse-DA reaction
of exo-3b–d (0.05 M) at 60 °C in CDCl3 monitored by 1H NMR, Figure S11: Time course for reverse-DA reaction
of exo-3b–d (0.03 M) in the presence of TFA (0.03 eq) at 60 °C in CDCl3 monitored by 1H NMR, Figure S12:
HPLC analysis of racemic exo-3b, Figure S13: HPLC analysis of 40% ee of exo-(-)-3b, Figure S14: HPLC analysis
of racemic of exo-3c, Figure S15: HPLC analysis of 98% ee of exo-(-)-3c, Figure S16: HPLC analysis of racemic
of exo-3d, Figure S17: HPLC analysis of 49% ee of exo-(-)-3d, Figure S18: 1H NMR spectrum of maleimide 2b,
Figure S19: 13C NMR spectrum of maleimide 2b, Figure S20: 1H NMR spectrum of maleimide 2c, Figure S21:
13C NMR spectrum of maleimide 2c, Figure S22: 1H NMR spectrum of maleimide 2d, Figure S23: 13C NMR
spectrum of maleimide 2d, Figure S24: 1H NMR spectrum of maleimide 2e, Figure S25: 13C NMR spectrum
of maleimide 2e, Figure S26: 1H NMR spectrum of maleimide 2f, Figure S27: 13C NMR spectrum of maleimide 2f,
Figure S28: 1H NMR spectrum of maleimide 2g, Figure S29: 13C NMR spectrum of maleimide 2g, Figure S30:
1H NMR spectrum of maleimide 2h, Figure S31: 13C NMR spectrum of maleimide 2h, Figure S32: 1H NMR
spectrum of maleimide 2i, Figure S33: 13C NMR spectrum of maleimide 2i, Figure S34: 1H NMR spectrum of
maleimide 2j, Figure S35: 13C NMR spectrum of maleimide 2j, Figure S36: 1H NMR spectrum of exo-3a, Figure S37:
13C NMR spectrum of exo-3a, Figure S38: 1H NMR spectrum of exo-3b, Figure S39: 13C NMR spectrum of exo-3b,
Figure S40: 1H NMR spectrum of exo-3c, Figure S41: 13C NMR spectrum of exo-3c, Figure S42: 1H NMR spectrum
of endo-3d, Figure S43: 13C NMR spectrum of endo-3d, Figure S44: 1H NMR spectrum of exo-3e, Figure S45:
13C NMR spectrum of exo-3e, Figure S46: 1H NMR spectrum of endo-3f, Figure S47: 13C NMR spectrum of endo-3f,
Figure S48: 1H NMR spectrum of exo-3g, Figure S49: 13C NMR spectrum of exo-3g, Figure S50: 1H NMR spectrum
of endo-3h, Figure S51: 13C NMR spectrum of endo-3h, Figure S52: 1H NMR spectrum of exo-3i, Figure S53:
13C NMR spectrum of exo-3i, Figure S54: 1H NMR spectrum of endo-3j, Figure S55: 13C NMR spectrum of endo-3j.

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