Research Article

Experimental and Numerical Investigation of Temperature Development of Ohmic Heating Cured Nonmass Concrete under Subzero Temperature

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In this paper, carbon fiber/carbon nanofiber strengthening nonmass concrete slab was designed, and ohmic heating (OH) curing was used to promote the strength formation of the slab under −20°C. COMSOL multiphysical field coupling program has been used to simulate the heating process of nonmass concrete slabs under different conditions. COMSOL analysis results showed that the optimal loading power density of OH cured sample under −20°C was 1000 W/m² ∼ 1200 W/m². Moreover, numerical analysis results were experimentally validated by the multipoint temperature measurement method. Furthermore, the mechanical properties showed that the compressive strength of the sample cured by 2 days OH curing at −20°C reached up to 48.2 MPa. SEM analysis exhibited that OH curing could improve the interfacial transition zone (ITZ) between the fiber and the matrix, leading to a denser microstructure. This study proved that COMSOL program could provide good theoretical guidance for OH cured nonmass cement concrete under subzero temperature. This work establishes an accurate guideline for electric power supplementation, laying a solid foundation of winter construction with high efficiency and low energy consumption.

1. Introduction

Concrete is a common material, which has attracted wide attention in the construction industry due to its low cost and excellent mechanical properties. However, cementitious materials fail to hydrate under subzero temperature conditions. Therefore, the preparation of concrete structures under subzero temperature is still a serious problem. As a result, the concrete construction in cold region in winter is greatly restricted, which affects the economic development. Traditional curing methods for winter concrete construction mainly include thermal insulation curing and external heating curing method [1, 2]. These methods have been utilized to protect concrete structure from being frozen. However, these methods only can be utilized under moderate conditions and will bring some unpreventable problems. To be specific, external heating curing method works by heating the air around the structure or directly heating the concrete. It is hard to operate and requires much energy consumption. Thermal insulation curing is conducted by covering heating preservation material on the concrete to slow down the heat release. This method is easy and inexpensive to achieve, while it is not suitable for the cold environment with the temperature lower than −10°C [3]. Thus, there is an urgent need for developing a new curing method for curing cementitious materials under ultra-low temperature that is energy-saving and environmentally friendly to meet the structural strength requirements [4, 5].
Ohmic heating (OH) curing method utilizes the ohmic heating generated by the action of electric current to cure cementitious materials. At present, a series of research results proved that OH curing could improve the strength formation of cement-based materials. Kovtun [6, 7] utilized direct current for OH curing of alkali activated cementitious materials containing fly ash under positive temperature. Temperature development was found to be closely related to the formation of strength with different voltage gradient conditions. However, with the progress of hydration, the electric conductivity of the cementitious materials degraded without the addition of conductive fillers, resulting in the decrease of the curing temperature [8]. Under this circumstance, Liu [9] cured cementitious materials incorporated with carbon nanofibers (CNFs) as conductive fillers with 12 h OH curing at −20°C and successfully raised the compressive strength of the sample to 27.7 MPa above the critical frost resistance strength of 3.5 MPa. Furthermore, Liu [10] conducted OH curing on the CF/CNFs reinforced cementitious composites under ultra-low temperature. The compressive strength of the sample reached up to 49.2 MPa with 2 days OH curing under −20°C. Above all, the previous work has solidly shown that OH curing method can be used as a novel and effective curing method for concrete construction under subzero temperature.

However, main researches on OH curing of cementitious materials under subzero temperature focused on the mechanical properties and hydration degree of small size concrete samples (such as 40 mm × 40 mm × 160 mm); the researches on OH cured nonmass concrete structures are still blank. However, the study regarding the properties of nonmass concrete slab has been investigated a lot due to its significance [11]. To be specific, based on the maturity theory of strength development on cement-based materials, the temperature development inside the sample under subzero temperature is crucial to ensure the sufficient strength formation of the sample [12, 13]. According to heat transfer theory, the heating process of small size structure can be regarded as a uniform heating process because of its low internal temperature gradient. However, for the cementitious materials with larger size and different geometries (such as nonmass concrete slab), the internal temperature gradient of the sample cannot be ignored, and the structure is more likely to suffer damage during OH curing process because of the large thermal expansion coefficient differences among the complicated components inside the sample [14–16]. Therefore, it is of vital significance to clarify the regularity of temperature development and corresponding influencing factors of OH cured nonmass concrete structures under subzero temperature. Also, it is essential to establish a numerical model to predict the temperature development of the structure.

COMSOL multiphysical field coupling program based on the solution of partial differential equations has been utilized widely to analyze realistic physical phenomena. For OH curing process, the modeling process is mainly based on Maxwell’s equations and fundamental principles of heat transfer. OH curing process is considered to be the application of electrothermal on concrete structure, and COMSOL program has been widely utilized in the field of electrothermal applications and concrete structure. To be specific, Zandi et al. [17] utilized COMSOL program to simulate the photogeneration, electrical properties, and heat distribution of graphene oxide contacting perovskite solar cells and effectively established the three-dimensional model of photo-electric-thermal and determined the promoting effect of graphene on the heating efficiency. Moreover, Li et al. [18] utilized COMSOL program to simulate the heating temperature development of external geothermal bridge system and the results were compared with the field test results. It was found that the simulated results were verified to accurately reflect the bridge heating efficiency in actual winter environment. Larwa et al. [19] simulated the heat flux and temperature distribution of phase change materials enhanced radiant floor systems by 2D model constructed by COMSOL program; it was verified that the utilization of COMSOL program could effectively reflect the heating situation of the system. In summary, COMSOL program can be expected to establish the relationship between different physical fields, especially in the electrothermal physical field. Therefore, COMSOL program has been utilized in this work to establish the model of heat distribution and temperature development within concrete structures cured by OH curing, so as to guide the OH curing process of concrete structures and promise the reasonable temperature distribution under subzero temperature.

In this paper, carbon fibers (CFs) have been utilized as macroscopic conductive fillers and CNFs were utilized as microscopic conductive fillers to synergistically prepare nonmass CFs/CNFs reinforced concrete slab (CFs/CNFs-CS) with the size of 350 mm × 450 mm × 40 mm. COMSOL multiphysical field coupling program was utilized to establish the numerical prediction model of the temperature development and distribution of OH cured slab under subzero temperature. The effects of different influencing factors including loading power densities, environmental temperature, and structure geometric shape on the temperature development and distribution were discussed in detail. Moreover, the temperature development and distribution of the OH cured slab at −20°C were experimentally measured to verify the accuracy of the numerical model. In addition, the mechanical properties of the OH curing nonmass CFs/CNFs-CS samples with optimized loading electric power were measured and SEM analysis was conducted to observe the microstructure of the samples.

2. COMSOL Multiphysical Field Coupling Numerical Simulation

The mutual coupling calculation among different physical fields (such as electric field and heat transfer field) can be realized by the COMSOL multiphysical field coupling program. In this work, OH curing process of nonmass concrete structure is closely related to the curing temperature and the environmental temperature, and the heat generation process is considered to be a transient process. Under this circumstance, COMSOL program was conducted to simulate the OH curing process of CFs/CNFs-CS under
subzero temperature. The detailed modeling process is shown as follows:

1. Definition of material parameters: the parameters of concrete structure provided by COMSOL database have been utilized to define some relevant parameters.

2. Establishment of physical field: the OH curing process is a Joule heating process, thus the Joule heating module in COMSOL has been selected, which includes current module and transfer module of solid heating. The current module has also been used to calculate the electric field distribution, current distribution, and potential distribution in the samples cured by OH curing. Based on Ohm’s law, the current conservation equation which utilizes scalar potential as the dependent variable has been solved. Its formula [20, 21] is shown as follows:

\[ \nabla \cdot J = Q_{\text{j,v}}, \]

\[ J = \sigma E + \frac{\partial D}{\partial t} + J_{\text{e}}, \]  

\[ E = -\nabla V, \]

where \( J \) is the current density vector (A/m²); \( Q_{\text{j,v}} \) represents the general current source (A/m³); \( E \) represents the intensity of the electric field (N/C); \( \sigma \) represents the conductivity (S/M); \( V \) is the electric potential; and \( D \) represents the relative dielectric constant (C2).

The features provided by the solid heating transfer module interface have been utilized to simulate the process of conduction convection and radiation heat transfer through heat flux and the surface settings of environmental radiation, in which, heat flux is defined as convection heat flux, and its expression [22, 23] is shown as follows:

\[ Q_{\text{D}} = h(T_{\text{ext}} - T), \]  

where \( Q_{\text{D}} \) is the convective heat transfer; \( T_{\text{ext}} \) represents the external temperature; and \( T \) is the temperature of the sample cured by OH curing. In this simulation, \( h \) represents the coefficient of heat transfer.

The transfer of radiant heat is defined by the surface to environment radiation module, and its hypothesis equation [24, 25] is as follows:

\[ Q_{\text{F}} = \varepsilon \sigma_{1} A (T_{\text{ext}} - T), \]  

where \( \varepsilon \) is the surface emissivity of the sample, which is also known as the blackness of the sample, the blackness of concrete value is 0.94; \( \sigma_{1} \) represents the Boltzmann constant with the value of \( 5.67 \times 10^{-8} \) W/(m²·K²); and \( A \) is the surface area of the sample.

Electromagnetic-thermal module has been selected to conduct modeling analysis during the COMSOL process of multiphysical field coupling; electromagnetic-thermal module is selected to conduct modeling analysis on the multiphysical field coupling of samples under OH curing condition. Its transient response hypothesis equation [26] is shown as follows:

\[ \rho C_{p} \frac{\partial T}{\partial t} + \rho C_{p} u \cdot \nabla T = \nabla \cdot (k \nabla T) + Q_{\text{e}}, \]  

where \( \rho \) is the density of the sample; \( C_{p} \) is the constant pressure heat capacity of the sample (J/(kg · K)); \( u \) is the vector field constructed; and \( K \) is the thermal conductivity (W/(m · K)).

3. Division of mesh grid: conventional grid division has been adopted. The size of the cuboid model is 350 mm × 450 mm × 40 mm, and the size of the cylinder model is 200 mm × 1200 mm. The complete grid of the model consists of “1465” domain cells, 600 boundary elements, and 80 edge cells with the condition of conventional grid division. The results of cuboid model mesh division are shown in Figure 1(a), and the results of cylinder model mesh division are shown in Figure 2(a).

4. Boundary conditions: the interface potential of one side has been set to be 0 in the current boundary conditions, and the electric potential of the opposite section is set to be Vtot, which is converted according to the power required by the experiment. The rest of the interfaces are set to be electrical insulation. The potential distribution diagram of the cuboid model is shown in Figure 1(b), and the potential distribution diagram of the cylinder model is shown in Figure 2(b). As shown below, the red area is considered as of high potential and the blue area is considered to be of low potential.

Solid heat transfer boundary conditions:

1. It is assumed that the relevant material parameters (specific heat capacity, the coefficient of conductivity, and the conductivity) of the sample cured by OH curing remain unchanged during the process of heat transfer.

2. Due to the low environmental temperature, no insulation layer is set, and all of the sections in the geometric model are considered to participate in the process of heat exchange.

5. Output of calculation results: the temperature development of the samples cured by OH curing is considered to be a transient process, the temperature of the sample changes consistently with time, thus the research is determined to be transient. In this work, the length of calculation step was set to be 0.5 min, and the calculation time was set to be 600 min. The temperature probe was set at the center point of the model to record the temperature development during OH curing process.
In this paper, COMSOL multiphysical field coupling program has been utilized to simulate OH cured samples under subzero temperature. The temperature development and heating regularity of the sample cured by OH curing under different environmental temperatures, different loading powers, and different sample sizes were mainly studied. The specific physical property parameters of materials used in the simulation process are shown in Table 1.

### 3. Materials and Experimental Method

#### 3.1. Materials

The cementitious material used in this experiment is PO 42.5 cement. The chemical composition of the cement is shown in Table 2. The aggregate is fine quartz sand with the particle size range of 0.11–0.21 mm, the fineness modulus of fine silica sand is 2.41. CFs produced by Japan Toray have been chosen as the conductive filler; the diameter and the length of CFs are 7 μm and 4 mm, respectively. Detailed physical properties of CFs are shown in Table 3. CNFs have been utilized to construct microscopic conductive paths and the length and average diameter of CNFs are 20 nm and 100 nm, respectively.

#### 3.2. Sample Preparation and OH Curing Procedures

In this experiment, the mix design of CFs/CNFs-CS is as follows: the ratio of water to cement is 0.3, the ratio of sand to cement is 1:1, the CFs addition amount is 0.75 vol%, and the volumetric addition of CNFs is 0.2 vol%. The detailed fabrication process of the samples has been listed as follows: firstly, CNFs and fine silica sand were put into the stirring
pot, and the CNFs were dispersed by rapid stirring with an eggbeater. Secondly, cement and CFs were sequentially placed in the pot, and the mixture was slowly stirred for 1 min with the mortar mixer and then stirred at high speed for 2 min to fully disperse CFs. Thirdly, the mixed solution of polycarboxylate superplasticizer (SP) and water was slowly added into the stirring pot and stirred for another 3 min to obtain final products. Finally, the mixture was poured into the plastic molds with the size of 350 mm × 450 mm × 40 mm embedded with two copper electrodes. The samples were then surface-smoothed and covered with plastic films. Two-electrode method was used to measure the resistance of CFs/CNFs-CS, the diagram of resistance measurement is depicted in Figure 3, and the resistivity $\rho$ is computed using the formulation as follows:

$$\rho = \frac{RS}{L},$$

in which $R$ is the measured resistance; $S$ represents the cross-sectional area of the composite; and $L$ is the distance between copper electrodes.

At the same time, fifteen thermocouples were arranged to record the temperature development of CFs/CNFs-CS sample cured by OH curing under subzero temperature. The diagram of the arrangement of thermocouples is shown in Figure 4. Moreover, the newly prepared sample was placed in a refrigerator with the constant temperature of $-20^\circ$C. To promise the stability of the power $P$, the voltage was adjusted according to the measured resistivity value every two hours complying with the following equation:

$$P = \frac{SU^2}{L\rho},$$

in which $P$ is the electric power; $U$ represents the voltage; $\rho$ represents the resistivity; and the cross-sectional area of the sample and the distance between the electrodes are denoted with $S$ and $L$, respectively.

### 3.3. Characterization and Test

The effects of different influencing factors on the temperature development and heating forms can be obtained by COMSOL program. The optimal loading electric power density of OH curing was determined and further utilized to prepare CFs/CNFs-CS sample under $-20^\circ$C to verify the accuracy of modeling results from the aspect of experiments. CFs/CNFs-CS samples with the size of 350 mm × 450 mm × 40 mm were cured by OH curing with the temperature of $-20^\circ$C for 1 day and 2 days to figure out the effect of OH curing on strength formation under subzero temperature. While CFs/CNFs-CS samples were also cured by room temperature (RT) curing (with the temperature of 20°C, humidity more than 95%) for 1 day and 2 days, after the curing procedure, the cuboid sample with the size of 40 mm × 40 mm × 160 mm was cut from the middle of the slab. The compressive strength measurement of the samples (40 mm × 40 mm × 160 mm) was manufactured according to ISO679:1989 and GB/T 17671-1999 with the loading rate of 2400 ± 200 N/s. The hydration process was terminated by immersing the small pieces of the samples into absolute ethanol. The small pieces were further cold dried for 6 h at $-60^\circ$C. Scanning electron microscopes (SEM, Hitachi, 9 SU5000) were utilized to obtain the morphology information of the microstructure in CFs/CNFs-CS samples.

### 4. Results and Discussion

#### 4.1. Numerical Analysis on the Effects of Different Influencing Factors on the Temperature Development and Distribution

In this section, numerical prediction model has been established by COMSOL program to simulate the temperature development and distribution of OH cured CFs/CNFs-CS samples with different influencing factors. The effects of loading power density, environmental temperature, and structure geometric shape are taken into consideration.
4.1.1. Loading Power Density. The temperature development of CFs/CNFs-CS samples is significantly affected by the loading electrical power density. The cuboid model with the geometric size of 350 mm × 450 mm × 40 mm was simulated, and the domain point probe was arranged at the center of the model with the coordinates of (175, 225, 20). The temperature distribution of the model after 600 min has been analyzed under different loading power densities (0 W/m², 200 W/m², 400 W/m², 600 W/m², 800 W/m², 1000 W/m², 1200 W/m², and 1400 W/m²). The results of simulation are shown in Figure 5 and the specific central temperatures of the samples are listed in Table 4. As shown in Figure 5, with the environmental temperature of −20°C, the temperature of the sample with the loading power density of 0 W/m² is always at subzero temperature, and this curing temperature cannot promise the hydration reaction of cementitious materials. However, with the loading power density of 200 W/m², 400 W/m², 600 W/m², and 800 W/m², the final curing temperatures at the center point of the sample reach around 10°C, 27°C, 45°C, and 60°C, respectively. It is worth mentioning that a proper curing temperature is essential to promise ongoing hydration process of cement-based materials [27, 28], leading to the sufficient strength formation, and at these temperatures, although the hydration reaction of concrete can be ensured, the promotion effect on its strength is not obvious. Moreover, with the loading power density of 1400 W/m², the peak temperature of the sample reaches up to 110°C. This high curing temperature may lead to the decomposition of ettringite inside the sample, resulting in the degradation of mechanical properties for the sample [29, 30]. Finally, with the loading power density of 1000 W/m² and 1200 W/m², the final curing temperature at the center of the sample can reach up to 80°C and 90°C, respectively. With these curing temperatures, the strength of the samples can be formed rapidly and the mechanical properties of the samples will not be affected [31, 32]. In conclusion, the optimal loading power density range of OH cured slabs at −20°C has been determined to be 1000 W/m² ∼ 1200 W/m².

![Figure 5: The simulated temperature at center point of the samples with different loading power densities.](image)

**Table 4: Simulated central temperatures of the samples with different loading power densities at 600 min.**

| Power density (W/m²) | 0 | 200 | 400 | 600 | 800 | 1000 | 1200 | 1400 |
|----------------------|---|-----|-----|-----|-----|------|------|------|
| Central temperature (°C) | −20 | 10 | 27 | 43 | 61 | 80 | 91 | 108 |

4.1.2. Environmental Temperature. The environmental temperature also has a great influence on the samples cured by OH curing under ultra-low temperature. The temperature in northern China can reach up to −40°C in winter. Therefore, it is necessary to simulate the temperature development of samples cured with different environmental temperatures. In this section, the loading power density has been determined to be 1000 W/m² to analyze the temperature distribution of the model with different environmental temperatures (0°C, −10°C, −20°C, −30°C, and −40°C), and the results are shown in Figure 6. It can be seen from Figure 6 that with the loading power density of 1000 W/m², the curing temperature of the sample can be maintained at 70°C ∼ 80°C with the environmental temperature range of −20°C ∼ −40°C at the age of 600 min. However, when the environmental temperature is between −10°C and 0°C, the peak temperatures of samples can reach up to 85°C ∼ 90°C. The hydration reaction of cementitious materials can be accelerated by properly increasing the curing temperature; this simulation result proves that OH curing can be utilized for concrete construction at severe cold regions in winter with the help of COMSOL numerical analysis.

![Figure 6: The simulated temperature at the center point of the sample with different environmental temperatures.](image)
4.1.3. Structure Geometric Shape. After the modeling and prediction of the cuboid model, it can be concluded that OH curing can be guaranteed by adjusting the loading power density to reach the proper curing temperature of the sample under subzero temperature. In this section, in order to enhance the application of COMSOL program, the temperature field distributions of both cuboid model and cylinder model with the environmental temperature of −20°C and the loading power density of 1000 W/m² were simulated, respectively. The size of the cuboid model is 350 mm × 450 mm × 40 mm, and the size of the cylinder model is Φ200 mm × 1200 mm. The simulation results are shown in Figures 7 and 8. It can be seen from Figure 7 that with the loading power density of 1000 W/m², the center temperature of the cuboid model is fairly high, while the temperature decreases gradually from the center point and the temperatures at four corners of the model exhibit lowest values. This phenomenon is due to that the four corners have the largest contact surface with the outside, thus the temperature at the corner decreases quicker. The cylinder model shows the same temperature distribution regularity, the temperature at the center of the sample is high, and the temperature far away from the central area gradually decreases. Moreover, with the increase of temperature, the temperature difference between the central region and the edge area becomes larger. When the curing time exceeds 200 min, the temperature gradually tends to be stable, and the temperature is uniformly distributed in most areas of the whole cylinder. It can be concluded that COMSOL numerical analysis can be utilized to simulate the temperature development of the samples cured by OH curing under subzero temperature with different volumetric shapes.

4.2. OH Curing of Nonmass CFs/CNFs-CS Sample Slab under Ultra-Low Temperature. In the above discussion, the influence of different factors on the temperature distribution of OH cured CFs/CNFs-CS samples has been analyzed by COMSOL program. In order to further confirm the accuracy of simulation analysis, experiments were carried out to investigate the temperature development of CFs/CNFs-CS. The curing temperature of the samples can reach up to 80–90°C with the loading power density of 1000 W/m²−1200 W/m², which has been proved in the previous section. In this section, the loading power density has been determined to be 1100 W/m² to promise the proper curing temperature; based on this, the applied electrical power has been set to be 30W. Moreover, the arrangement of the thermocouples in the experiment is shown in Figure 4.

The distributions of temperature field have been recorded numerically and experimentally, and the results are respectively shown in Figures 9 and 10. Figure 9 exhibits the temperature distribution at the measured points of OH cured CFs/CNFs-CS sample at −20°C at the first 500 min curing duration. It can be seen that the temperature development regularity of each point is almost same with the applied electrical power of 30 W, indicating the uniform distribution of conductive paths constructed by CFs/CNFs. To be more specific, the curing temperature of CFs/CNFs-CS...
sample cured by OH curing increases obviously and reaches up to the peak temperature at 400 min. However, the peak temperatures at different measured points seem to have little difference. The peak temperature at the center point of the sample is about 75–80°C, while the peak temperature from the edge area exhibits lower value of 52–60°C. In conclusion, the temperature at the center of the sample is generally higher than that around the sample. The reason for this difference is that the heat transfer path of the edge area is shorter than that of the central area. This causes that the heat dissipation speed is faster at the edge area of the sample compared with that at the central area of the sample [33, 34].

Figure 10 shows the temperature distribution of CFs/CNFs-CS sample simulated by COMSOL program. The peak temperature at the central area of the sample is about 85–88°C, while the peak temperature at the edge area is 60–70°C with the loading power density of 1100 W/m². Moreover, it takes 100 minutes with the heating rate of 0.68°C/min for the peak temperature at the central area of the sample to raise from 20°C to 88°C by numerical simulation, while it takes 400 minutes with the heating rate of 0.15°C/min for the actual center temperature to rise from 20°C to 80°C by experimental measurement. It can be concluded that the temperature and heating rates simulated by COMSOL program are a little higher and faster than the measured temperature and heating rate during OH curing, and this is considered to be the reason that the actual curing condition of OH cured sample is much more complicated than the simulated environment. For example, the resistivity of the sample changed all the time during the curing process, leading to the actual applied power being always lower than the simulated power.

To further compare the curing temperatures of the samples, the peak temperature distribution of CFs/CNFs-CS sample measured numerically and experimentally is listed in Table 5. It can be seen from Table 5 that the whole temperature field simulated by COMSOL program is symmetrical distribution. The peak temperature at the center area is the highest, and the peak temperature gradually decreases with the increase of the distance from the center point. Moreover, it can be seen that the temperature prediction at the center of the sample is close to that of the actual OH cured sample, indicating the accuracy of the program. However, the peak temperature distribution of the sample cured by OH curing at 20°C is not as uniform as that obtained by the simulation analysis, but it still conforms to the temperature distribution regularity. This is considered to be that although CFs and CNFs could construct conductive paths inside the sample, the distribution of CFs/CNFs is not completely uniform, and there is still a certain gap of heating uniformity between the simulation analysis and actual experiment. However, the peak temperature of CFs/CNFs-CS sample cured by OH curing can reach up to 55–80°C at −20°C. This curing temperature is sufficient to promise the proper curing condition of the sample under ultra-low temperature by promoting the hydration reaction of cementitious materials to a great extent. Therefore, the developed simulation program is promising to guide the winter construction of nonmass cementitious materials cured by OH curing under ultra-low temperature.

4.3. Mechanical Properties. As shown in Figure 11, the compressive and flexural strengths of the samples cured with different curing conditions were measured. It can be seen from Figure 11(a) that the compressive strength of the samples cured by 1 day OH curing at −20°C reaches up to 34.3 MPa, which is much greater than the critical frost resistance strength of 3.5 MPa. Moreover, it is also much higher than that of the sample cured by 1 day RT curing (19.7 MPa). Further, the compressive strength of 2 days OH cured CFs/CNFs-CS sample also increases obviously with the value of 48.2 MPa compared with that of the sample cured by 2 days RT curing (38.1 MPa). This shows that the compressive strength of the sample can be significantly improved by OH curing with the electrical power of 30 W at −20°C.

Figure 11(b) represents the flexural strengths of CFs/CNFs-CS samples cured with different conditions. The results indicate the flexural strengths of the samples developed in the same regularity as the compressive strengths. As shown in Figure 11(b), the flexural strength of 1 day OH cured sample is 10.5 MPa, which is much higher than that of the sample cured with 1 day RT curing (6.7 MPa). Moreover, the flexural strength of the sample subjected to 2 days OH curing reaches up to 11.5 MPa, which is 22.3% higher than that of the samples with 2 days RT curing.

4.4. SEM Analysis. SEM analysis of CFs/CNFs-CS samples subjected to different curing conditions was conducted and the results are shown in Figure 12. It can be seen from
| Simulated temperature (°C) at different points | 1  | 2  | 3  | 4  | 5  | 6  | 7  | 8  |
|-----------------------------------------------|----|----|----|----|----|----|----|----|
| 1                                            | 88.35 | 61.05 | 71.97 | 71.95 | 61.09 | 60.09 | 72.09 | 71.97 |
| 2                                            | 97.28 | 11.12 | 12.13 | 13.14 | 15.1 | 16.17 | 18.19 | 19.1 |
| 3                                            | 1  | 2  | 3  | 4  | 5  | 6  | 7  | 8  |
| 4                                            | 61  | 72.82 | 72.82 | 86.49 | 86.49 | 86.5 | 86.48 | 86.49 |

| Measured temperature (°C) at different points  | 1  | 2  | 3  | 4  | 5  | 6  | 7  | 8  |
|-----------------------------------------------|----|----|----|----|----|----|----|----|
| 1                                            | 80.5 | 56.2 | 63.5 | 68.1 | 57.6 | 54.1 | 69.7 | 70.9 |
| 2                                            | 61.1 | 74.3 | 72.2 | 75.9 | 76.4 | 75.4 | 79  | 80  |

**Table 5:** Peak temperatures of the samples measured numerically and experimentally.

![Mechanical properties of CF/CNF-CS samples](image)

**Figure 11:** Mechanical properties of CF/CNF-CS samples. (a) Compressive strength and (b) flexural strength.

![SEM morphology](image)

**Figure 12:** (a) SEM morphology of samples cured by 2 days RT curing with a magnification of 2000x, and the samples cured by 2 days OH curing with the magnifications of (b) 2000x, (c) 5000x, and (d) 10,000x.
Figure 12(a) that the sample cured by 2 days RT curing exhibits relatively loose microstructure, and the surface of CFs are fairly smooth. However, the implementation of 2 days OH curing is beneficial for the microstructure of the samples. To be specific, a much denser microstructure can be found in 2 days OH cured samples, as shown in Figure 12(b). Moreover, hydration products inside the sample exhibit a trend to attach onto the surface of CFs, which can refine the ITZ between CFs and the matrix, and this is beneficial for mechanical properties of the samples. Figures 12(a) and 12(b) respectively display the distribution situation of CFs and CNFs in the samples. A uniformly distributed situation of CNFs can be observed from Figures 12(a) and 12(b). This is beneficial to the stability of OH curing of the samples. In addition, the distribution situation of CNFs has been displayed in Figures 12(c) and 12(d); it is shown that CNFs can uniformly distribute in the sample to construct conductive network from the microscopic point of view. Based on the above microstructure evidences, it can be concluded that 2 days OH curing with 30 W electrical power is beneficial to the strength development of the CFs/CNFs-CS samples compared with 2 days RT curing.

5. Conclusion
This work numerically establishes the relationship between loading power and the curing temperature of the samples cured by OH curing, leading to the accurate guideline of applied power. This lays a solid foundation for concrete construction at cold region with high efficiency and low energy consumption. Detailed conclusions have been shown as follows:

1. The numerical simulation results of COMSOL program show that the loading power and environmental temperature have a close influence on the curing temperature of nonmass CFs/CNFs-CS. Higher loading power and environmental temperature can lead to higher curing temperature. Moreover, the optimal loading power density of the sample calculated by COMSOL program is determined to be 1000 W/m²–1200 W/m² at −20°C, and this loading power density can help the temperature at the central region of CFs/CNFs-CS sample reach up to 86–88°C in theory.

2. The peak temperature of CFs/CNFs-CS sample reaches to 80.5°C at −20°C with the loading electrical power of 30 W in the experimental measurement, which is very close to the numerical results. This proves the good prediction effect of COMSOL numerical program. Moreover, the simulated temperature field is symmetrical, and the temperature decreases from the center to the corner of the sample. The temperature field measured by the experiment basically conforms to this regularity.

3. The compressive strengths of OH cured CFs/CNFs-CS samples for 1 day and 2 days are increased by 74.11% and 26.5%, respectively, compared with those of the samples cured by 1 day and 2 days RT curing. Moreover, the flexural strengths of the samples cured by OH curing for 1 day and 2 days reach up to 10.5 MPa and 11.5 MPa, respectively. In addition, the results of SEM analysis show that the CFs/CNFs-CS samples cured by OH curing exhibit denser microstructure and better anchor situation between fibers and the matrix.

Data Availability
The raw data used to support the findings of this study are available from the corresponding author upon request.

Conflicts of Interest
The authors declare that they have no conflicts of interest.

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