Evaluation of Improved Model to Accurately Monitor Soil Water Content

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Abstract: The accurate monitoring of soil water content during the growth of crops is of great importance to improve agricultural water use efficiency. The Campbell model is one of the most widely used models for monitoring soil moisture content from soil thermal conductivities in farmland, which always needs to be calibrated due to the lack of adequate original data and the limitation of measurement methods. To precisely predict the water content of complex soils using the Campbell model, this model was evaluated by investigating several factors, including soil texture, bulk density and organic matter. The comparison of the R² and the reduced Chi-Sqr values, which were calculated by Origin, was conducted to calibrate the Campbell model calculated. In addition, combining factors of parameters, a new parameter named m related to soil texture and the organic matter was firstly introduced and the original fitting parameter, E, was improved to an expression related to clay fraction and the organic matter content in the improved model. The soil data collected from both the laboratory and the previous literature were used to assess the revised model. The results show that most of the R² values of the improved model are >0.95, and the reduced Chi-Sqr values are <0.01, which presents a better matching performance compared to the original. It is concluded that the improved model provides more accurate monitoring of soil water content for water irrigation management.

Keywords: soil water monitoring; improved model; irrigation; agriculture water efficiency

1. Introduction

Currently, more than 70% of agricultural water resources around the world are occupied by field crop irrigation [1,2], while the global average irrigation efficiency is only 50% [3–5]. Especially in China, the irrigation water use efficiency is only 30~40% [6,7], which is even lower than the worldwide level. The main factor of low irrigation efficiency is that the soil water content of farmland cannot be accurately monitored, which leads to irrationality in the formulation of the irrigation system, and it is impossible to accurately irrigate, resulting in wasted water resources over time. Wealth production and industrial growth are inseparable from the efficient use of water resources in agriculture [8,9], and it is important to accurately monitor soil water in real time, which helps to formulate a reasonable irrigation plan for realizing automated irrigation, increasing the irrigation water utilization coefficient, and optimizing the reasonable distribution of water resources [10–14].

Several methods of monitoring soil water content have been researched, such as time domain reflectometry, gravimetric sampling [15,16], the remote sensing measurement, the neutron detector method, and so on [17]. Among them, the prediction of soil moisture content from soil thermal properties has attracted the attention of many scholars [18–22].
The relationship between thermal characteristics and soil moisture can not only accurately estimate the soil moisture content, but also be helpful to explore the laws of soil water movement. The most widely used empirical model to determine soil water content based on thermal conductivity was presented by Campbell [20], which was applied in many later studies and instrument developments [23–25].

However, due to the complexity of field crops and soil conditions, as well as the differences in soil properties in each region, the estimated results of the Campbell model have been proven to have large errors in many cases [26,27]. The internal factors refer to the properties of the soil itself (such as its texture and composition [28]). Additionally, the external factors are those that can be controlled artificially, such as the porosity and organic matter content [29,30].

Researchers have analyzed and explored the Campbell model in multiple directions, and found that it is greatly affected by soil texture, compaction, and organic matter content, and large errors have occurred in estimating the water content of various types of soil [31,32]. Mahdavi et al. found the Campbell model was affected by the degree of compaction and the particle shape [33]. Wallen et al. explored the influence of soil texture on the Campbell model and proposed that the model needs to be improved [34]. Zhao et al. found that the Campbell model has large errors in the estimation of soil moisture content and thermal conductivity under high organic matter content and high temperature [35].

Some researchers have tried to calibrate the data estimated by the Campbell model for specific soil [11,34,36], but no improvement plan was proposed for the Campbell model to expand the applicable soil range. Therefore, focusing on the influencing factors of the Campbell model and improving its coefficients to accurately monitor water content of different soils will be of great importance to improve the efficiency of soil moisture monitoring. To improve the accuracy of soil water content evaluated from soil thermal conductivities by the Campbell model, this study investigated several influencing factors to assess the error of the $\lambda$–$\theta$ curve simulated by the Campbell model. In addition, the coefficients of the Campbell model were revised to reduce the error and the improved model was evaluated by the soil data from both laboratory and previous studies.

2. Materials and Methods

2.1. Soil Description

Ten soil samples with different geological conditions taken from various farmlands across five provinces of China including Jiangsu, Shandong, Hunan, Yunnan and Sichuan were measured in this study in the State Key Lab of Hydrology—Water Resources and Hydraulic Engineering, Hohai University, China. The particle size of soil distribution was determined by the pipette method [37] and classified according to the USDA standards, and the bulk density was determined by the cutting ring method [38]. The organic matter content was measured by the Automated Dry Combustion (ADC) method [39] and the total salt content of the soil was determined by the mass method [40]. These 10 soil samples are used to construct different test groups and verify the final modified model. Table 1 lists the raw soil characteristics.

| Sample Code | Type of Soil       | Texture | Organic Matter | Salinity | Bulk Density |
|-------------|--------------------|---------|----------------|----------|--------------|
|             |                    | Sand    | Silt | Clay | %  | g cm$^{-3}$  |              |
| Soil 1      | Sand               | 90      | 8   | 2   | 0.04 | 0.031 | 1.35        |
| Soil 2      | Loamy sand         | 78      | 21  | 1   | 0.89 | 0.041 | 1.36        |
| Soil 3      | Loamy sand         | 79      | 14  | 7   | 0.16 | 0.122 | 1.49        |
| Soil 4      | Loamy sand         | 76      | 13  | 11  | 0.01 | 0.083 | 1.45        |
Table 1. Cont.

| Sample Code | Type of Soil | Texture | Organic Matter | Salinity | Bulk Density |
|-------------|--------------|---------|----------------|----------|--------------|
|             |              | Sand    | Silt | Clay | %     | g cm$^{-3}$ |
| Soil 5      | Loam         | 20      | 70   | 10   | 0.53  | 1.42 |
| Soil 6      | Sandy loam   | 62      | 21   | 17   | 0.22  | 1.37 |
| Soil 7      | Loam         | 49      | 31   | 20   | 1.25  | 1.47 |
| Soil 8      | Silt loam    | 12      | 65   | 23   | 3.50  | 1.56 |
| Soil 9      | Clay loam    | 52      | 15   | 33   | 1.60  | 1.54 |
| Soil 10     | Clay         | 25      | 15   | 60   | 0.92  | 1.49 |

2.2. Experiment Design

2.2.1. Sample Preparation for Evaluating the Campbell Model

To research the influencing factors of the Campbell model, the experiments were divided into three parts, each of which corresponds to one factor. This study adopted the controlled variable method and soils from Table 1 were chosen to be prepared into proper samples for research purposes. All prepared soil samples were placed in a cylindrical aluminum box (30 mm of height and 50 mm of diameter), and each prepared soil sample had five parallel samples. Each soil sample was tested three times and the average value was taken.

When studying the influence of soil texture, the selection and process of soils 1, 4, 5, 6, and 10 were according to the largest bulk density, organic matter, and salt content, which ensured that other factors, except soil composition, were in the same condition. Soil samples were air-dried and sieved before being filled into an aluminum box. According to the organic matter content of 0.92% and the salt content of 0.083%, peat moss and NaCl were mixed into the sample. When the bulk density was less than the set 1.55 g cm$^{-3}$, the triaxial compression was used to ensure that the physical properties of the soil sample other than the particle composition are maintained.

When exploring the influence of bulk density, soil 1 was chosen due to its small initial bulk density, which can be compressed to prepare soil samples with larger bulk densities. Soil 1 was air-dried and sieved before being placed in the aluminum boxes. Since the volume of the aluminum box was fixed, it was necessary to weigh different qualities of Soil 1 and compress them into aluminum boxes with the triaxial compression instrument [41].

When researching the influence of the organic matter, considering the interaction of clay content on soil organic matter [42], and when studying organic matter content as the influencing factor, soils with different textures were studied separately. Soils 1 and 10 were chosen to be prepared and peat moss was used as additional organic matter to provide different organic matter fraction samples [43]. After the soil was air-dried and sieved, peat moss was mixed into the soil sample according to five set organic content levels of 0.04%, 0.2%, 0.8%, 1.6%, and 3.0% [36,44]. After that, the bulk density was re-measured and adjusted to ensure that every sample was in the same bulk density state.

Table 2 lists the basic properties of soil samples to explore the influencing factors of the $\lambda\sim\theta$ model.
Table 2. Soil samples for evaluating the factors influencing the Campbell model.

| Influencing Factors | Sample Code | Type of Soil | Texture | Organic Matter | Salinity | Bulk Density | % | g cm⁻³ |
|---------------------|-------------|--------------|---------|----------------|----------|--------------|---|--------|
|                     |             |              | Sand    | 90             | 8        | 2            |   |        |
|                     |             |              | Silt    | 76             | 13       | 11           |   |        |
|                     |             |              | Clay    | 20             | 70       | 10           | 0.92| 0.09 | 1.55 |
|                     |             |              | Loam    | 62             | 21       | 17           |   |        |
|                     |             |              | Clay    | 25             | 15       | 60           |   |        |
|                     | S          | Sand         |         |                |          |              | 1.35|       |
|                     | LS         | Loamy sand   |         |                |          |              | 1.45|       |
|                     | SLL        | Silt Loam    |         |                |          |              | 1.55|       |
|                     | SDL        | Sandy loam   |         |                |          |              | 1.60|       |
| Bulk density        | BD1.35     | Sand         |         |                |          |              |    | 1.35  |
|                     | BD1.45     |              |         |                |          |              |    | 1.45  |
|                     | BD1.50     |              |         |                |          |              |    | 1.55  |
|                     | BD1.55     |              |         |                |          |              |    | 1.60  |
|                     | BD1.60     |              |         |                |          |              |    |       |
|                     | SOM0.04    | Sand         |         |                |          |              | 0.04|       |
|                     | SOM0.2     |              |         |                |          |              | 0.2 |       |
|                     | SOM0.8     |              |         |                |          |              | 0.8 |       |
|                     | SOM1.6     |              |         |                |          |              | 1.6 |       |
|                     | SOM3.0     |              |         |                |          |              | 3.0 |       |
|                     | COM0.04    | Sand         |         |                |          |              | 0.04|       |
|                     | COM0.2     |              |         |                |          |              | 0.2 |       |
|                     | COM0.8     |              |         |                |          |              | 0.8 |       |
|                     | COM1.6     |              |         |                |          |              | 1.6 |       |
|                     | COM3.0     | Clay         |         |                |          |              | 3.0 |       |
| Organic matter      |             | Clay         |         |                |          |              | 0.015| 1.49 |
|                     |             |              |         |                |          |              | 0.16 |       |

2.2.2. Calibration of the Revised Model

Soils listed in Table 1 were prepared to calibrate the revised model. After being dried and sieved, each kind of soil was weighed into five equal parts and placed in aluminum boxes according to a consistent operation process, that is, there were five parallel samples of each kind of soil. Water with different quality was added and mixed. Measurements were conducted from five different locations of each sample to average the error of measurement of thermal conductivities. The relationship curve between soil thermal conductivity and water content was drawn and compared with the improved model.

2.2.3. Soil Thermal Properties and Water Content Measurement

The thermal conductivities of the soil throughout the entire experiment were measured using a KD2 Pro. The thermal conductivity detector KD2 Pro developed by Decagon has been proven to be relatively highly accurate by many researchers [45,46]. Additionally, the data measured by the KD2 Pro were used to represent the actual thermal conductivities [47].

To show the influence of these factors on the model curve more intuitively, the method of actively adding water was adopted to obtain a quantitative soil water value, so that the disturbance of organic matter and salinity during each drying process could be avoided. For each set of experiments, the same quality of water was mixed into each aluminum box at the same time. All the samples were sealed with plastic wrap for 24 h. During the water injection process, the soil was completely filled in the aluminum box, and each sample weighed again to avoid the overflow of solid materials due to the injection of water.

2.3. Evaluation Methods

2.3.1. The Campbell Model

In 2010, the Campbell model was used to explore the feasibility of optical fiber for distributed soil water measurement [48], which provided a theoretical basis for the real-time monitoring of soil water status, automatic irrigation, and field management [49]. Since soil thermal conductivity is an inherent property of soil and even water is constantly changing,
Campbell takes soil water as the independent variable and soil thermal conductivity as the dependent variable. The model expression and the parameters are as follows:

$$\lambda = A + B\theta - (A - D) \exp \left[ - (C\theta)^E \right]$$  \hspace{1cm} (1)

The coefficient $A$ is determined by the volume fraction of quartz and other minerals:

$$A = \frac{0.57 + 1.73\phi_q + 0.93\phi_m - 2.8\phi_s(1 - \phi_s)}{1 - 0.74\phi_q - 0.49\phi_m - 2.8\phi_s}$$  \hspace{1cm} (2)

where $\phi_q$ is the volume fraction of quartz, $\phi_m$ is the volume fraction of other minerals and $\phi_s$ is the solid fraction of the soil, which equals the sum of $\phi_q$ and $\phi_m$. The coefficients $B$, $C$, $D$, and $E$ are given as

$$B = 1.06\rho_b$$  \hspace{1cm} (3)

$$C = 1 + \frac{2.6}{\phi_{clay}^{1/2}}$$  \hspace{1cm} (4)

$$D = 0.03 + 0.1\rho_b^2$$  \hspace{1cm} (5)

$$E = 4$$  \hspace{1cm} (6)

where $\rho_b$ is the bulk density of the soil and $\phi_{clay}$ is the clay content, and the particle density of mineral soil is assumed to be 2.65 g cm$^{-3}$. The parameters $B$ and $D$ are determined by the bulk density of the soil, $C$ is associated with the clay content, which determines the water content where the thermal conductivity starts rising rapidly, and $E$ is the fitting parameter of the curve [20].

It can be seen that the parameters in the Campbell model, except for the parameter $E$, have certain physical meanings and are closely related to various influencing factors. By analyzing the error trend in the Campbell model curve under each influencing factor, the parameters that need to be improved can be preliminarily judged.

2.3.2. Error Analysis

This study uses $R^2$ and the reduced Chi-Sqr calculated by Origin to analyze the error between the Campbell model curve and the measured curve under each influencing factor. The $R^2$ represents the fit of the Campbell model curve to the measured value. The closer the $R^2$ is to 1, the better the fit. The reduced Chi-Sqr represents the error between the simulated curve and the measured curve [50]. When the reduced Chi-Sqr approaches 0, the error of the simulated value becomes smaller [51].

Since it is difficult to control the thermal conductivity of the soil at the same level, the study chose to verify the error between the simulated value and the measured value of the soil thermal conductivity under the same moisture content, and performed a linear fitting, of which the $R^2$ represents the fitting spend.

3. Results

3.1. Campbell Model Implications

In this part, the $\lambda$-$\theta$ curve of the measured soil samples with the Campbell model curve and quantitatively analyzed error was compared. The Campbell model also gives detailed anatomy in terms of parameter assignment, and corrections were made based on the factors influencing the parameters.

3.1.1. Among Soil with Different Textures

For soil with a specific texture, the thermal conductivity increases rapidly as the soil water content increases (Figure 1). The response shows two stages. When the water content is higher than a certain level, which is generally 0.05–0.1 m$^3$ m$^{-3}$, the rate gradually declines with the increase in soil thermal conductivity.
Among soils with different textures, the growth rate of thermal conductivity for sandy soil with low water content is significantly greater than that of clay soil. On a full range of water content, the thermal conductivity of coarse-grain soil for any water content is greater than that of fine-grain soil due to the high proportion of quartz [52].

The Campbell [20] model almost matched the measured data of soil sample S when the water content was <0.1 (m$^3$ m$^{-3}$) and that of sample C when the water content was <0.2 (m$^3$ m$^{-3}$). The thermal conductivities predicted by the Campbell model are always lower than the measured values, which implies that the parameters that determine the degree of increase in the model curve need to be adjusted. At full water content, $R^2$ varies in the range 0.722–0.876, with a low degree of matching and a large range. The reduced Chi-Sqr tends to decrease as the soil clay content increases (Table 3). Thus, soil texture has a great impact on the $\lambda$–$\theta$ curve, and the Campbell model showed different trends under soils with different textures, which is consistent with the research conclusion of Wallen et al. [34]. It is assumed that the error of the model curve comes from the parameters of the soil texture.

Table 3. Reduced Chi-Sqr and $R^2$ of the measured value and the Campbell model simulation value for soils with different textures.

| Soil Code | Reduced Chi-Sqr | $R^2$  |
|-----------|----------------|--------|
| S         | 0.190          | 0.722  |
| LS        | 0.097          | 0.781  |
| SLL       | 0.104          | 0.777  |
| SDL       | 0.028          | 0.783  |
| C         | 0.027          | 0.876  |

3.1.2. Among Soil with Different Bulk Densities

As is shown in Figure 2, when the water content was low (<0.05 m$^3$ m$^{-3}$), the difference between the $\lambda$–$\theta$ of soil samples with different bulk densities was very little. As the water content increases, the thermal conductivity of soil samples with larger bulk densities increases to a greater degree than that of soil samples with lower bulk density. The higher
the dry density of the soil, the more solid matter per unit volume of the soil and the closer the soil particles are arranged. Thus, the contact area between particles increases accordingly, which ultimately leads to an increase in the soil’s thermal conductivity.

Figure 2. The measured relationship of $\lambda$-$\theta$ and the curves estimated by the Campbell model for soil with different bulk densities. The colored dots represent the measured values and the dotted lines represent the Campbell model curves.

Compared with the Campbell model, $R^2$ varies in the range 0.652–0.732, which is far from 1, and the degree of matching is lower than that of the influence of soil texture (Table 4). This may be due to the fact that particle density in the Campbell model is assumed to be 2.65 g cm$^{-3}$, while the particle density of soils is actually in the range 2.6–2.8 g cm$^{-3}$ [53].

Table 4. Reduced Chi-Sqr and $R^2$ of the measured value and the Campbell model simulation value for soils with different bulk densities.

| Soil Code | Reduced Chi-Sqr | $R^2$ |
|-----------|-----------------|------|
| BD1.35    | 0.219           | 0.652|
| BD1.45    | 0.176           | 0.672|
| BD1.50    | 0.210           | 0.655|
| BD1.55    | 0.179           | 0.717|
| BF1.60    | 0.201           | 0.732|

Under different soil bulk density, the Campbell model curve is higher than the measured curve, that is, the influence of the soil bulk density on the Campbell model is monotonic, but because the degree of influence is less than the soil texture, it is not suitable to directly select the parameters that have a more obvious response to the curve shape for correction.

3.1.3. Among Soil with Different Organic Matter Contents

The empirical models proposed in the previous studies rarely consider the organic matter. To improve the model’s applicability and accuracy, the effects of organic matter on the model were studied with two soil texture types: sand and clay. The properties and the experimental results of samples are shown below (Figure 3).
Figure 3. The relationship of $\lambda$ vs $\theta$ and the curve estimated by the Campbell model for soil with different organic matter contents. Figure (a) shows the results of Soil 1, representing sandy soil. Figure (b) shows the results of Soil 10, representing clay soil.

For the sandy soil shown in Figure 3a, the soil sample with more organic matter has lower thermal conductivity for almost the entire range of water content. However, for clay soil (Figure 3b) with a low level of water content, the $\lambda$ of the soil sample with more organic matter is higher than the soil containing less organic matter. Additionally, as the water content increases, the $\lambda$ of the soil sample with more organic matter has a lower rate of increase and gradually becomes lower than that of samples with less organic matter.

The Campbell model does not consider the differences in soil organic matter content, that only one response model can be given for two different soil samples. In terms of the sandy soil sample, the simulation overall is small, and the $R^2$ decreases with the increase in organic matter content. For the clay soil, the model value is overall large, the deviation is greater at high water content, and the trend in $R^2$ is opposite to that of sandy soil (Table 5).

Table 5. Reduced Chi-Sqr and $R^2$ of the measured value and the Campbell model simulation value for soils with different organic matter contents.

| Soil Code | Reduced Chi-Sqr | $R^2$ | Soil Code | Reduced Chi-Sqr | $R^2$ |
|-----------|----------------|-------|-----------|----------------|-------|
| SOM0.04   | 0.193          | 0.792 | COM0.04   | 0.037          | 0.748 |
| SOM0.2    | 0.176          | 0.766 | COM0.2    | 0.047          | 0.829 |
| SOM0.8    | 0.161          | 0.744 | COM0.8    | 0.045          | 0.872 |
| SOM1.6    | 0.144          | 0.731 | COM1.6    | 0.046          | 0.876 |
| SOM3.0    | 0.117          | 0.722 | COM3.0    | 0.050          | 0.892 |

The different responses of the Campbell model to organic matter on different texture soils illustrated that organic matter plays a different role for different soil textures. It can be explained that organic matter plays an important role in the water and heat coupling process [44]. Usowicz and Lipiec [29] analyzed the effect of biochar obtained from wood biomass and other organic amendments (peat and compost) on soil thermal properties and attributed the results to the addition of exogenous organic matter. In the performance of reduced Chi-Sqr and $R^2$, the $\lambda$ vs $\theta$ curve predicted by the Campbell model for cohesive soil was significantly better than that for sandy soil.

3.2. Summary of Error Sources in the Campbell Model Curve

1. Among the various factors, Campbell has the lowest match degree of soils with different bulk densities. Therefore, it may be necessary to focus on parameters related to bulk density. The soil texture and organic matter content will affect the particle
density of soil. In the Campbell model, the values of the parameters B and D default the soil particle density to 2.65 g/cm$^3$.

2. The organic matter not only reduces the density of soil particles but also interacts with clay particles in the soil, thereby affecting the parameters related to clay content in the Campbell model.

3. Various parameters have different influences on the shape of the model and the parameters for correction can be determined by changes in the shape.

4. Discussion

4.1. Revised Model

The Campbell model proved through experiments that there are unequal errors under various influencing factors that need to be corrected, which is also consistent with the conclusions of other scholars. The revised empirical model attempts to improve the accuracy of the $\lambda-\theta$ relationship evaluation and to expand the range of water content that can match this model.

In the curve of the Campbell model, the parameters, which are C, D, and E, are in an exponential expression. Among them, the parameter E is a fitting parameter with no actual physical meaning. Therefore, the correction of the parameter E was selected rather than the parameters C and D. If the parameter E is revised, the influence of the parameters C and D on the curve could be expressed at the same time, which makes it easier to obtain a convergent solution than revising three parameters at the same time when using the least squares method to fit [54]. At the same time, the correction parameter m is introduced and the original parameter B is corrected. Since the bulk density has a smaller effect on the curve than the soil texture, and a small change in parameter B will also have a greater effect on the curve, this study chose to introduce the parameter m. The revised empirical model was proposed as follows (Equation (7)):

$$\lambda = A + B\theta^m - (A - D) \exp \left[ -(C\theta)^E \right]$$

(7)

To find the determinants of the values of parameter m and E, Soil 1 was selected as an example to analyze the influence of different m and E values in the curve (Figure 4).

Parameter m affects the degree of curve rise. As the value of m approaches 1, the curve gradually flattens, the growth rate slows, and parameter m has an influence on the thermal conductivity value under the full range of water content. As parameter E increases, the rising part of the curve steepens. Furthermore, while parameter E determines the shape
of the curve when the volumetric water content is <0.3 m$^3$ m$^{-3}$, under high water content, changes in the value of parameter $n$ have few effects on the curve.

It is assumed that parameter $m$ is the matched option associated with the soil texture and organic matter and that parameter $E$, which replaced the parameter $E$ proposed by Campbell, was decided by the clay fraction and organic matter. The soil sample data were used to match the measured data using the software Originlab 2021. Table 6 shows the $m$ and $E$ values of each soil sample.

### Table 6. The values of $m$ and $E$ of the soil samples.

| Influencing Factors | Sample Code | $m$   | $E$   |
|---------------------|-------------|-------|-------|
| Texture             | S           | 0.468 | 1.211 |
|                     | LS          | 0.619 | 1.362 |
|                     | SLL         | 0.542 | 1.350 |
|                     | SDL         | 0.763 | 1.466 |
|                     | C           | 1.582 | 2.203 |
|                     | BD1.35      | 0.452 | 0.928 |
|                     | BD1.45      | 0.454 | 0.931 |
|                     | BD1.50      | 0.458 | 0.931 |
|                     | BD1.55      | 0.455 | 0.930 |
|                     | BF1.60      | 0.452 | 0.933 |
|                     | SOM0.04     | 0.452 | 0.931 |
|                     | SOM0.2      | 0.458 | 0.977 |
|                     | SOM0.8      | 0.479 | 1.164 |
|                     | SOM1.6      | 0.488 | 1.418 |
|                     | SOM3.0      | 0.514 | 1.854 |
|                     | COM0.04     | 2.111 | 2.659 |
|                     | COM0.2      | 2.119 | 2.595 |
|                     | COM0.8      | 2.133 | 2.237 |
|                     | COM1.6      | 2.146 | 1.789 |
|                     | COM3.0      | 2.172 | 1.001 |

For soil samples of different bulk densities, the values of parameter $m$ and $E$ are almost equal, which illustrates that the values of $m$ and $E$ have nothing to do with soil bulk densities. For soil samples with different textures, the values of parameter $m$ and $E$ tend to increase as the clay content increases. Regarding the influence of organic matter, the parameter $m$ values of sandy soil and clay soil both increase with the increase in organic matter content. However, the changing trend for parameter $E$ is the opposite. The parameter $E$ of sandy soil increases in proportion with the increase in organic matter content, while that of cohesive soil decreases.

Therefore, it is assumed that the value of parameter $m$ is related to soil texture and organic matter content, while parameter $E$ is only related to clay content and organic matter content. We used the least-squares method to obtain the expression of the parameters $m$ and $E$ (Equations (8) and (9)):

\[
m = 0.71\varphi_{sand} + 0.57\varphi_{silt} + 2.6\varphi_{clay} + 1.88\varphi_{om} - 0.28 \tag{8}
\]

\[
E = 3.07\varphi_{clay} + 34\varphi_{om} - 151\varphi_{clay}\varphi_{om} + 0.86 \tag{9}
\]

where $\varphi_{sand}$ is the sand fraction, $\varphi_{silt}$ is the silt fraction, $\varphi_{clay}$ is the clay fraction, and $\varphi_{om}$ is the organic matter fraction.

#### 4.2. Evaluation and Error Analysis

The model evaluation is conducted to prove the applicability of the revised model, including the range of water content. Here, two groups of data were used: the soil sample listed in Table 1 and the data from previous studies. The reduced Chi-Sqr and $R^2$ of the measured and modeled curve were used to evaluate the new model.
4.2.1. Model Evaluation by Laboratory Data

The comparison of soil thermal conductivity predicted by the Campbell model and the revised model that used data from the laboratory in Table 1 are as follows.

As depicted in Table 7, for other soils except Soil 9, compared with the Campbell model, the $R^2$ of the revised model is 0.001–0.012, which was much lower than 0.28–0.93 from the reduced Chi-Sqr of the original Campbell model. The $R^2$ values of the revised model are all >0.95, except for Soil 9. Soil 9 is clay loam with 0.244% salinity. The cause of this error would be the high value of the clay fraction [55]. Noborio and Mcinnes [36] suggested that clay particles interacted with salt, thereby affecting the soil’s thermal conductivity.

Table 7. Comparison of the reduced Chi-Sqr and $R^2$ of the Campbell model and the revised model on the measured soil in Table 1.

| Soil Code | Reduced Chi-Sqr | $R^2$        |         |         |
|-----------|-----------------|--------------|---------|---------|
|           | Campbell        | Revised      | Campbell| Revised |
| Soil 1    | 0.168           | 0.006        | 0.718   | 0.983   |
| Soil 2    | 0.178           | 0.012        | 0.803   | 0.982   |
| Soil 3    | 0.045           | 0.001        | 0.722   | 0.995   |
| Soil 4    | 0.077           | 0.002        | 0.782   | 0.988   |
| Soil 5    | 0.015           | 0.017        | 0.847   | 0.967   |
| Soil 6    | 0.022           | 0.002        | 0.84    | 0.987   |
| Soil 7    | 0.032           | 0.018        | 0.871   | 0.965   |
| Soil 8    | 0.073           | 0.004        | 0.792   | 0.991   |
| Soil 9    | 0.254           | 0.133        | 0.616   | 0.538   |
| Soil 10   | 0.045           | 0.002        | 0.912   | 0.981   |

Figure 5 shows that the measured values of other soils except Soil 9 and the predicted thermal conductivities of the revised model with the same water content are evenly distributed on both sides of the 1:1 line, that means the revised model has good predictions on laboratory data.

![Figure 5](image.png)

Figure 5. Comparison of predicted soil thermal conductivity ($\lambda$) values from the new model vs. measured data under the same water content of soils in Table 1.

4.2.2. Model Evaluation by Data from Previous Studies

Twelve groups of data from Lu et al. [56], were used to evaluate the improved model (Figure 6).
As shown in Table 8, for soil from previous studies, the reduced Chi-Sqr of the improved model was significantly smaller than that of the Campbell model. The measured soil thermal conductivities are evenly distributed on both sides of the 1:1 line. Moreover, the $R^2$ of the revised model is mostly >0.95. Among them, the $R^2$ of Lu 2 and Lu 6 were 0.872 and 0.893, respectively. It is assumed that these errors came from either the measurement process or interference in the salt content of the soil samples. However, their $R^2$ are still higher than those of the Campbell model, which improves the matching accuracy to a certain extent.

Table 8. Comparison of the reduced Chi-Sqr and $R^2$ of the Campbell model and the new model on the measured soil from Lu et al.

| Soil Code | Type of Soil | Texture | Organic Matter | Bulk Density | Reduced Chi-Sqr | $R^2$ |
|-----------|--------------|---------|----------------|--------------|----------------|------|
|           |              | Sand    | Silt | Clay | % | g cm$^{-3}$ | Campbell | Revised | Campbell | Revised |
| Lu1       | Sand         | 94      | 1    | 5    | 0.09 | 1.60 | 0.209 | 0.013 | 0.713 | 0.962 |
| Lu2       | Sand         | 93      | 1    | 6    | 0.07 | 1.60 | 0.202 | 0.017 | 0.782 | 0.872 |
| Lu3       | Sandy loam   | 67      | 21   | 12   | 0.86 | 1.39 | 0.060 | 0.006 | 0.741 | 0.976 |
| Lu4       | Loam         | 40      | 49   | 11   | 0.49 | 1.30 | 0.066 | 0.002 | 0.629 | 0.987 |
| Lu5       | Silt loam    | 27      | 51   | 22   | 1.19 | 1.33 | 0.022 | 0.006 | 0.844 | 0.956 |
| Lu6       | Silt loam    | 11      | 70   | 19   | 0.84 | 1.31 | 0.055 | 0.010 | 0.397 | 0.893 |
| Lu7       | Silty clay loam | 19   | 54   | 27   | 0.39 | 1.30 | 0.016 | 0.009 | 0.898 | 0.945 |
| Lu8       | Silty clay loam | 8    | 60   | 32   | 3.02 | 1.30 | 0.011 | 0.003 | 0.869 | 0.967 |
| Lu9       | Clay loam    | 32      | 38   | 30   | 0.27 | 1.29 | 0.004 | 0.000 | 0.969 | 0.997 |
| Lu10      | Silt loam    | 2       | 73   | 25   | 4.4  | 1.20 | 0.007 | 0.001 | 0.940 | 0.988 |
| Lu11      | Loam         | 50      | 41   | 9    | 0.25 | 1.38 | 0.082 | 0.002 | 0.670 | 0.993 |
| Lu12      | Sand         | 92      | 7    | 1    | 0.6  | 1.58 | 0.232 | 0.009 | 0.401 | 0.976 |
5. Conclusions

This study proposed a revised model of the relationship between soil water and thermal conductivity. The influence of soil texture, bulk density, and organic matter content on the $\lambda_\theta$ model was analyzed and the parameters that need to be improved which influenced the performance of the Campbell model were well evaluated.

Both laboratory and literature data proved that the revised model improved the accuracy of $\lambda_\theta$ relationship prediction and expanded the applicability of the model. However, this study was a laboratory experiment, completed by preparing soil samples, and the measurement of actual soil moisture generally requires in situ measurement. Whether the improved model can be used in in situ measurement needs further verification. The results also confirm that the revised model could not match the clay soil with a high salt concentration, which could be attributed to the interaction between clay and salt. However, for most texture and salt concentrations of soil, the revised model had higher accuracy and a wider applicable water content range than the original model. Moreover, although the revised model had improved accuracy, the calculation became more complicated and each parameter required a large amount of soil information. In the actual application process, it is necessary to use software, such as Matlab, to insert the model in the water monitoring system. The revised model is expected to provide greater service when applied to agricultural field water measurement to accurately obtain field water conditions, thereby increasing the irrigation water utilization coefficient.

Author Contributions: Writing and editing: J.J., Y.X.; experiment conducting: J.J., Y.L.; data processing: J.J.; conceptualization: J.X. All authors have read and agreed to the published version of the manuscript.

Funding: This study was funded by the State Key Laboratory of Hydrology Water Resources and Hydraulic Engineering through the Research Project 519042212—Hohai University.

Institutional Review Board Statement: Not applicable.

Informed Consent Statement: Not applicable.

Data Availability Statement: The data presented in this study are available on request from the corresponding authors. The data are not publicly available due to the continuation of a follow-up study by the authors.

Acknowledgments: Financial and instrument support provided by the State Key Laboratory of Hydrology Water Resources and Hydraulic Engineering of Hohai University.

Conflicts of Interest: The authors declare no conflict of interest.

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