Object-based Multipass InSAR via Robust Low Rank Tensor Decomposition

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Abstract—This is the pre-acceptance version, to read the final version please go to IEEE Transactions on Geoscience and Remote Sensing on IEEE Xplore.

The most unique advantage of multipass InSAR interferometry (InSAR) is the retrieval of long term geophysical parameters, e.g. linear deformation rates, over large areas. Recently, an object-based multipass InSAR framework has been proposed in [1], as an alternative to the typical single-pixel methods, e.g. Persistent Scatterer Interferometry (PSI), or pixel-cluster-based methods, e.g. SqueeSAR. This enables the exploitation of inherent properties of InSAR phase stacks on an object level. As a follow-on, this paper investigates the inherent low rank property of such phase tensors, and proposes a Robust Multipass InSAR technique via Object-based low rank tensor decomposition (RoMIO). We demonstrate that the filtered InSAR phase stacks can improve the accuracy of geophysical parameters estimated via conventional multipass InSAR techniques, e.g. PSI, by a factor of ten to thirty in typical settings. The proposed method is particularly effective against outliers, such as pixels with unmodeled phases. These merits in turn can effectively reduce the number of images required for a reliable estimation. The promising performance of the proposed method is demonstrated using high-resolution TerraSAR-X image stacks.

Index Terms—Object-based; InSAR; SAR; Low rank; Tensor decomposition; Iterative reweighting

I. INTRODUCTION

A. Multipass InSAR

Multipass or multibaseline InSAR techniques, such as persistent scatterer interferometry (PSI) [2]–[9], distributed scatterer interferometry [10]–[11], and differential SAR tomography (D-TomoSAR) [12]–[23], are the most popular methods for the retrieval of geophysical parameters (namely elevation and deformation parameters) for extended areas.

Past research on multipass InSAR was mainly focused on the optimal retrieval of the phase history parameters of individual scatterers, which can be considered in two categories: single-pixel-based methods and pixel-cluster-based methods.

On one hand, single-pixel-based methods, such as PSI [2]–[9], and D-TomoSAR [18]–[23], have been widely applied to the monitoring of urban areas. In particular, significant development has been made in D-TomoSAR, such as super-resolution D-TomoSAR methods based on Compressive Sensing (CS) [24]–[26], and combining D-TomoSAR with SAR geodesy [27], [28] to obtain absolute Geodetic TomoSAR [29] point clouds. On the other hand, pixel-cluster-based methods, such as SqueeSAR [12]–[14], [16], [30]–[32], CAESAR [33] and TomoSAR based on distributed scatterers [34]–[36], exploit statistical similarities between the neighboring pixels, in order to retrieve the phase history parameters from their associated covariance matrices. Statistical ergodicity of the selected pixel clusters is always assumed in these methods for the estimation of the required sample covariance matrix. Likewise, nonlocal-InSAR (NL-InSAR) [37]–[40] also selects similar pixels but based on patch similarity.

Although some of the abovementioned techniques do exploit information from multiple neighbouring pixels or patches, no explicit semantic and geometric information that might be preserved in the images has been utilized. In [41], Zhu et al. demonstrated that by introducing building footprints from OpenStreetMap (OSM) as prior knowledge of pixels sharing similar heights into frameworks based on joint sparse reconstruction techniques, a highly accurate tomographic reconstruction can be achieved using only six interferograms, instead of the typically-required 20-100. Inspired by this, we recently proposed a general framework for object-based InSAR deformation reconstruction based on a tensor-model with a regularization term, which is combined with semantic information shown in SAR images, i.e. classification labels of different objects like bridges, roofs and façades, for an improvement of deformation retrieval [1].

Based on the previous work, this paper seeks to investigate the inherent low rank property of multipass InSAR phase tensors, given semantic prior knowledge of objects. We propose a novel robust tensor decomposition method using iterative reweighting to recover an outlier-free phase stack for the retrieval of the geophysical parameters.

B. Low rank modeling

Low rank modeling has been applied in many research fields of data analysis, since high-dimensional data are often embedded in a low-dimensional subspace [43]. One of the best known low rank modeling approaches is Principle Component Analysis (PCA) [44], which finds a low rank version of the...
matrix by minimizing the approximation error to the original data matrix in a least-squares sense. It has been utilized for tackling various problems in remote sensing, such as SAR-image-based change detection [43], hyperspectral image denoising [46], data feature extraction [47], and so on. For applications in the InSAR field, PCA has recently been utilized for decomposing the scatterer covariance matrix in CAESAR [33], in order to separate layovered scatterers within individual pixels.

However, due to the assumption of independently and identically distributed (i.i.d.) Gaussian samples, PCA is sensitive to the existence of outliers. To robustly recover the low rank data matrix, [48] proposed Robust PCA (RPCA) to decompose the original matrix into a low rank data matrix and a sparse outlier matrix. For instance, RPCA was deployed for hyperspectral image restoration in [49], and a RPCA-based approach for separating stationary and moving targets in SAR imaging was investigated in [50]. To deal with the data in a multidimensional case, [51] proposed a robust low-rank tensor recovery method called Higher order RPCA (HoRPCA), which has been employed in our previous work [1] as an outlier filtering step for object-based InSAR deformation reconstruction.

C. Contributions of this paper

To this end, the contributions of this paper are three-fold:

- Based on the tensor model of object-based InSAR phase stacks [1], we study their multidimensional low rank property.
- With this prior knowledge, we propose a novel InSAR phase tensor low rank decomposition method using iterative reweighting, which is named as RoMIO.
- Using simulation and real data, we demonstrate that the InSAR phase stacks filtered by RoMIO can improve the accuracy of geophysical parameters estimated via conventional multipass InSAR techniques, e.g. PSI, by a factor of ten to thirty in typical settings, especially in the existence of outliers.

D. Structure of this paper

The rest of this paper is organized as follows. Section II studies the low rank property of such phase stacks. In Section III, the proposed RoMIO method is demonstrated for robustly recovering object-based InSAR phases. Experiments including simulated and real InSAR data are conducted to substantiate the performance of the proposed algorithm in Section IV. We discuss the experimental results in Section V. Section VI draws the conclusion of this paper.

II. LOW RANK PROPERTY OF INSAR PHASE STACKS

A. Tensor basics

A tensor can be considered as a multi-dimensional array. The \textit{order} of a tensor is the number of its \textit{modes} or \textit{dimensions}. A tensor of order $N$ in the complex domain can be denoted as $X \in \mathbb{C}^{I_1 \times I_2 \times \ldots \times I_N}$ and its entries as $x_{i_1,i_2,\ldots,i_N}$. Specifically, vector $x$ is a tensor of order one, and matrix $X$ can be represented as a tensor of order two. \textit{Fibers} are the higher-order analogy of matrix rows and columns, which are defined by fixing every index but one. \textit{Slices} of a tensor are obtained by fixing all but two indices. Matricization, also known as \textit{unfolding}, is the process of reordering the elements of a tensor into a matrix. Specifically, the mode-$n$ unfolding of tensor $X$ is defined by $X_{(n)}$ that is obtained by arranging the mode-$n$ fibers as the columns of the matrix. The utilized tensor notations are summarized in Table I. The detailed introductions about multilinear algebra are presented in [52], [53].

B. Tensor model of object-based multipass InSAR phase stacks

As proposed in our previous work [1], given object areas, such as façades, bridges or roofs, an InSAR phase stack can be represented by a 3-mode tensor: $G \in \mathbb{C}^{I_1 \times I_2 \times I_3}$, where $I_1$ and $I_2$ represent the spatial dimensions in range and azimuth, and $I_3$ denotes the number of SAR images. The phase tensor of the object can be modeled by

$$G(S, P) = \exp\{-j\left(\frac{4\pi}{\lambda r} S \otimes b + \frac{4\pi}{\lambda} P \otimes \tau\right)\},$$

where $G$ is the modeled phase tensor of the object, $b \in \mathbb{R}^{I_3}$ is the vector of the spatial baselines, $\tau \in \mathbb{R}^{I_3}$ is a warped time variable [21], e.g. $\tau = t$ for a linear motion, and $\tau = \sin(2\pi(t-t_0))$ for a seasonal motion model with temporal baseline $t$ and time offset $t_0$. $S \in \mathbb{R}^{I_1 \times I_2}$ and $P \in \mathbb{R}^{I_1 \times I_2}$ are the unknown elevation and deformation maps to be estimated, respectively. $\lambda$ is the wavelength of the radar signals and $r$ denotes the range between radar and the observed object. The symbol $\otimes$ denotes the outer product [53]. A simulated example of such a phase stack is illustrated in Figure 1. It shows the wrapped phase stack, and the simulated linear
deformation rates and elevations from which the phase stack is constructed. The pattern of the simulated elevation map is comparable to that of urban objects in real scenarios. The simulated deformation map shows a more complex pattern, which represents continuously varying displacement in the scene. The elevation and deformation maps are designed to be spatially uncorrelated.

Such phase tensors in urban areas usually experience an inherent low rank nature, since it can be generally assumed that $S$ and $P$ follow certain regular structure or homogeneous pattern, because of the regular man-made structures in urban areas. Moreover, the observed SAR images of urban object areas are usually highly correlated along the temporal dimension. Such low rank property will be demonstrated and investigated in the following chapter.

C. Low rank study of InSAR phase stacks

Since PCA is the most basic low rank decomposition method for matrices, it will be employed in this section to demonstrate the low rank property of InSAR phase tensor. PCA is usually realized by Singular Value Decomposition (SVD) [54]. Given a matrix $X \in \mathbb{C}^{I_1 \times I_2}$ and its SVD, i.e. $USV^H$, the rank $R$ approximation of $X$ by truncating $S$ up to $R$ dominant singular values is the matrix $X_R = UR_SV_R^H$, where the $R \times R$ diagonal matrix $S_R$ satisfies $S_R(i,i) = \frac{1}{\sqrt{\sigma_i}}$, where $\sigma_i$ are the singular values of $X$, and $V_R$ consists of the first $R$ rows of $V$. This is also known as truncated SVD.

As a higher-dimensional extension of SVD, Higher order Singular Value Decomposition (HoSVD), also known as Tucker decomposition [55], can provide a tensor data compression based on the low rank approximation, as illustrated in Figure 2. It decomposes a tensor into a core tensor multiplied by a matrix along each mode. Specifically, for a 3-mode tensor, $X_{I_1 \times I_2 \times I_3}$, we have

$$X = S \times_1 U \times_2 V \times_3 W,$$

where $U = I_{I_1 \times R_1}$, $V = I_{I_2 \times R_2}$, and $W = I_{I_3 \times R_3}$ are the factor matrices that can be considered as the principle components in each mode [52]. $S \times_1 R_{1 \times R_2 R_3}$ is the so-called core tensor, and $\odot$ is mode-$n$ multiplication between tensor and matrix [53]. $(R_1, R_2, R_3)$ is the so-called multilinear rank of $X$. They fulfill the inequalities $R_1 \leq \min(I_1, I_2 I_3)$, $R_2 \leq \min(I_2, I_1 I_3)$, and $R_3 \leq \min(I_3, I_1 I_2)$.

A low rank approximation of $X$ can be realized by the truncated HoSVD. Take $X_{I_1 \times I_2 \times I_3}$ as an example, we can define its tensor approximation with multilinear rank $(K_1, K_2, K_3)$, where $K_1 \leq R_1$, $K_2 \leq R_2$, $K_3 \leq R_3$, by the following truncated HoSVD:

$$X^1_{I_1 \times I_2 \times I_3} \approx S_{K_1 \times K_2 \times K_3} \times_1 U^1_{I_1 \times K_1} \times_2 V^1_{I_2 \times K_2} \times_3 W^1_{I_3 \times K_3},$$

where $U^1 = I_{I_1 \times K_1}$, $V^1 = I_{I_2 \times K_2}$ and $W^1 = I_{I_3 \times K_3}$ are created by storing the first $K_i (i = 1, 2, 3)$ singular vectors of $U$, $V$ and $W$ and replacing the left $R_i - K_i (i = 1, 2, 3)$ vectors by zeros, and $S_{K_1 \times K_2 \times K_3}$ is created in a similar way. Such truncated HoSVD finds a low rank tensor approximation of the original tensor $X$ in a least-squares sense.

In order to investigate the low rank property of an InSAR phase tensor, the normalized singular values ($\sigma_i/\max(\sigma_i)$) of the mode-1, -2 and -3 unfolding matrices of a simulated noise-free complex-valued phase tensor $\tilde{G} \in \mathbb{C}^{100 \times 100 \times 50}$ (shown in Figure 1) are plotted in Figure 3. It can be observed that the singular values of the three unfolding matrices decay rapidly, which indicates the low rank nature of the original tensor. The low rank tensor approximation $\hat{G}$ of $\tilde{G}$ can be obtained by the truncated HoSVD with a predefined threshold. As shown in Figure 4, we calculate the Mean Square Error (MSE) values of the real-valued residual phases between the approximated tensor $\hat{G}$ and the original tensor $\tilde{G}$, i.e. $\text{MSE}(|\angle(\hat{G} \odot \text{conj}(\tilde{G})))$, with respect to different thresholds, where $\odot$ denotes the element-wise product and

| TABLE I | Mathematic notations |
|-----------------|---------------------|
| $\mathcal{X}$, $X$, $x$, $x$ | tensor, matrix, vector, scalar |
| $X^{(n)}$ | mode-$n$ unfolding of tensor $X$ |
| $(R_1, R_2, \cdots, R_N)$ | tensor multilinear rank, where $R_n = \text{Rank}(X^{(n)})$, $n = 1, 2, \cdots, N$ |
| $\langle X, Y \rangle$ | inner product of tensor $X$ and $Y$, i.e. the sum of product of their entries |
| $\|X\|_F$ | Frobenius norm of tensor $X$, i.e. $\|X\|_F = \sqrt{\langle X, X \rangle}$ |
| $\text{vec}(X)$ | vectorization of $X$ |
| $\|X\|_1$ | $L_1$ norm of tensor $X$, i.e. $\|X\|_1 = \|\text{vec}(X)\|_1$ |
| $\|X\|_2$ | matrix nuclear norm: the sum of its singular values, i.e. $\|X\|_2 := \sum \sigma_i$ |
| $Y = X \times_n A$ | mode-$n$ multiplication of tensor $X$ and matrix $A$, i.e. $Y^{(n)} = AX^{(n)}$ |
| $\odot$ | outer product |
| $\odot$ | element-wise product |
normalized singular value

MSE value (rad²)

MSE of the real-valued residual phases w.r.t. threshold values

Fig. 3. Plots of the normalized singular values of mode-1, -2 and -3 unfolding matrices of the simulated example of the complex-valued InSAR phase stack shown in Figure 4. For visualization, we just plot the first 40 out of all the 128 normalized singular values of mode-1 and -2 unfolding matrices. It is demonstrated that the singular values of the three unfolding matrices decay rapidly, which indicates the low rank structure of the original tensor.

Fig. 4. The Mean Square Error (MSE) values of the real-valued residual phases between the low rank approximated tensor Š and the original tensor Š, i.e. MSE(angle(Š ⊙ conj(Š))) w.r.t different threshold values.

Fig. 5. An InSAR phase tensor example of TerraSAR-X data with a roof area (blue rectangle) of LasVegas convention center. For the illustration, we show the amplitudes of the multipass SAR images.

\( \text{conj}(\cdot) \) is the complex conjugate operator. According to the plot, the original InSAR phase stack can be well approximated by the low rank tensor Š with acceptable errors. For example, at the thresholding value of 0.21, the MSE value of the real-valued residual phases between Š (its multilinear rank is \((11, 12, 5)\)) and Š is around 0.01 [rad²], which is equivalent to an uncertainty of 0.2 [μm/year] in linear deformation rate or 0.69 [m] in elevation at the baseline configuration of the simulated data. Such low rank property is often embedded in images. This is especially true in urban areas where man-made objects with regular shapes are abundant.

Such low rank property also exists in real data which usually contains full rank noise. To this end, the normalized singular values of an experimental TerraSAR-X phase tensor with a roof area (Figure 5) are demonstrated in Figure 6. The associated phase tensor has the dimensions of \(256 \times 320 \times 29\). It can be seen that the normalized singular values decay rapidly and most of them are below \(0.2\), which indicates the low rank structure of the InSAR phase tensor.

III. ROBUST PHASE RECOVERY VIA ITERATIVELY REWEIGHTED TENSOR DECOMPOSITION

For the case of real data, outliers, e.g. unmodeled phases, usually exist in the observed phase stack. To tackle this challenge, we propose a novel robust tensor decomposition method — robust iteratively reweighted tensor decomposition.

A. Robust low rank tensor decomposition

Different from HoSVD where the approximation error is minimized in a least-squares sense, robust low rank tensor decomposition minimizes the rank with \( L_0 \) norm of the approximation error

\[
\{ \hat{X}, \hat{E} \} = \arg \min_{X,E} \text{rank}(X) + \gamma \|E\|_0, \quad \text{s.t. } X + E = G, \quad (4)
\]

where \( G \) is the observed InSAR phase tensor, \( E \) models the tensor of sparse outliers, \( \hat{X}, \hat{E} \) are the recovered outlier-free phase tensor and the estimated outlier tensor, respectively, \( \text{rank}(X) \) refers to the multilinear rank of \( X \), \( \|E\|_0 \) denotes the \( L_0 \) norm of \( E \), i.e. \( \|E\|_0 = ||\text{vec}(E)||_0 \), and \( \gamma \) is the regularization parameter.

This problem is NP hard, due to the minimization of the multilinear rank and the \( L_0 \) norm. Regarding this, [51] suggested to replace (4) by the following convex optimization problem

\[
\{ \hat{X}, \hat{E} \} = \arg \min_{X,E} \|X\|_* + \gamma \|E\|_1, \quad \text{s.t. } X + E = G. \quad (5)
\]
It relaxes the tensor multilinear rank to the tensor nuclear norm $\|\mathbf{X}\|_*$ which is the sum of the $N$ nuclear norms $\sum_n \|\mathbf{X}(n)\|_*$ of the mode-$n$ unfoldings of $\mathbf{X}$, i.e. $\|\mathbf{X}\|_* = \sum_n \|\mathbf{X}(n)\|_*$, and by replacing the tensor $L_0$ norm with the convex $L_1$ norm, i.e. $\|\mathbf{E}\|_1 = \|\text{vec}(\mathbf{E})\|_1$. This is known as HoRPCA which is a tensor extension of the matrix RPCA [48].

B. Robust Iteratively Reweighted Tensor Decomposition

In order to better approximate the rank of a matrix and the $L_0$ norm of a vector, [56], [57] proposed a reweighted nuclear norm and $L_1$ minimization scheme by enhancing the low rank and sparsity simultaneously during the optimization. The reweighted $L_1$ norm is defined as $\|w \odot x\|_1$, where $w$ is the weight vector that updates adaptively for enhancing the sparsity of $x$. It is worth noting that if each element of $w$ is exactly the inverse absolute value of the corresponding element of $x$, i.e. $w_i = \frac{1}{|x_i|}$, the reweighted $L_1$ norm equals the $L_0$ norm of $x$, i.e. $\|\frac{1}{|x|} \|_1 = \|x\|_0$. For the low rank enhancement, the nuclear norm for matrix $\mathbf{X}$ is replaced by a reweighted version $\|w \odot \mathbf{X}\|_1$. Likewise, if we have $w_i = \frac{1}{\sigma_i(\mathbf{X})}$, then the reweighted nuclear norm turns into the rank of the matrix $\mathbf{X}$, i.e. $\|w \odot \mathbf{X}\|_1 = \text{rank}(\mathbf{X})$.

Inspired by this, we extend the reweighting scheme to the tensor case. By introducing the weights for enhancing the low rank of $\mathcal{X}$ and the sparsity $\mathcal{E}$, the optimization problem is

$$\{\hat{\mathcal{X}}, \hat{\mathcal{E}}\} = \arg\min_{\mathcal{X}, \mathcal{E}} \sum_{n=1}^{N} \|w_{\mathcal{L},n} \odot \sigma(\mathbf{X}(n))\|_1 + \gamma \|\mathcal{W}_\mathcal{E} \odot \mathcal{E}\|_1$$

subject to $\mathcal{X} + \mathcal{E} = \mathcal{G}$, (6)

where $w_{\mathcal{L},n}$ is the weight vector for the singular values of the mode-$n$ unfolding matrix $\mathbf{X}(n)$, and $\mathcal{W}_\mathcal{E}$ is the weight tensor for $\mathcal{E}$. Note that if all weights are set to 1, (6) will be equivalent to (5).

C. Optimization by Alternating Direction Method of Multipliers (ADMM)

The optimization problem [5] can be solved by the ADMM framework [58]. The constraint optimization problem in (4) is firstly converted to its augmented Lagrangian function, yielding

$$L_\mu(\mathcal{X}, \mathcal{E}, \mathcal{Y}) = \sum_{n=1}^{N} \|w_{\mathcal{L},n} \odot \sigma(\mathbf{X}(n))\|_1 + \gamma \|\mathcal{W}_\mathcal{E} \odot \mathcal{E}\|_1 - \langle \mathcal{Y}, \mathcal{X} + \mathcal{E} - \mathcal{G} \rangle + \frac{1}{2\mu} \|\mathcal{X} + \mathcal{E} - \mathcal{G}\|_F^2,$$ (7)

where $\mathcal{Y}$ denotes the introduced dual variable and $\mu$ is the penalty parameter. ADMM takes advantage of splitting one difficult optimization problem into several subproblems, where each of them has a closed-form solution. Accordingly, the minimization of $L_\mu$ with respect to each variable can be solved by optimizing the following subproblems:

1) $\mathcal{X}$ subproblem: By fixing $\mathcal{E}$ and $\mathcal{Y}$, the subproblem of $L_\mu$ with respect to $\mathcal{X}$ can be rewritten as

$$\min_{\mathcal{X}} \sum_{n=1}^{N} \|w_{\mathcal{L},n} \odot \sigma(\mathbf{X}(n))\|_1 + \frac{1}{2\mu} \|\mathcal{X} + \mathcal{E} - \mathcal{G}\|_F^2.$$ (8)

This subproblem can be solved by the Nonuniform Singular Value Thresholding (NSVT) operator [57], [59]. Taking matrix $\mathbf{A}$ as an example, given the thresholding weight vector $w$, NSVT is defined as $T_w(\mathbf{A}) := \text{UDiag}(\text{max}(\sigma_i - w_i, 0)) \mathbf{V}$, with $U$, $V$ and $\sigma_i$ calculated by SVD of $\mathbf{A}$.

2) $\mathcal{E}$ subproblem: By fixing $\mathcal{X}$ and $\mathcal{Y}$, the subproblem of $L_\mu$ with respect to $\mathcal{E}$ has the following form

$$\min_{\mathcal{E}} \gamma \|\mathcal{W}_\mathcal{E} \odot \mathcal{E}\|_1 + \frac{1}{2\mu} \|\mathcal{X} + \mathcal{E} - \mathcal{G}\|_F^2.$$ (9)

This weighted $L_1$-norm optimization subproblem can be solved by the Nonuniform Soft Thresholding (NST) operator, which is defined as $S_{\mathcal{W}}(\mathcal{A}) := \text{sign}(\mathcal{A}) \odot \text{max}(|\mathcal{A}| - \mathcal{W}, 0)$, with $|\mathcal{A}| = \text{sign}(\mathcal{A}) \odot \mathcal{A}$.

3) $\mathcal{Y}$ updating: The dual variable $\mathcal{Y}$ can be updated by

$$\mathcal{Y} = \mathcal{Y} - \frac{1}{\mu} (\mathcal{X} + \mathcal{E} - \mathcal{G}).$$ (10)

4) Weight updating: The weight vector $w_{\mathcal{L},n}, n = 1, \ldots, N$ and the weight tensor $\mathcal{W}_\mathcal{E}$ can be updated by

$$w_{\mathcal{L},n} = \frac{1}{\sigma(\mathbf{X}(n)) + \epsilon}, \quad \mathcal{W}_\mathcal{E} = \frac{1}{|\mathcal{E}| + \epsilon}.$$ (11)
where $\epsilon_C$ and $\epsilon_E$ are the predetermined positive constants.

The detailed ADMM pseudocode for solving (6) is summarized in Algorithm 1.

Using a predefined convergence condition, the solution $(\hat{X}, \hat{E})$ can be obtained, i.e., the outlier-free InSAR phase tensor and the sparse outlier tensor, respectively. To this end, by applying conventional multipass InSAR techniques, e.g., PSI [2] on $X$, we can robustly retrieve the geophysical parameters.

Algorithm 1 RoMIO solved by ADMM

Input: $G, \gamma, \mu, N, \epsilon_C = \epsilon_E = 1 \times 10^{-3}$
1: Initialize $X^{(0)} = E^{(0)} = Y^{(0)} = 0$
2: for $k = 0$ to $k_{\text{max}}$ do
3: NSVT on the mode-$n$, $n = 1, \ldots, N$ unfolding of $G + \mu Y^{(k)} - E^{(k)}$, then, folding mode-$n$ tensors and averaging them by $N$

\[ X^{(k+1)} \leftarrow \frac{1}{N} \sum_{n=1}^{N} T_{n,\mu} N W_{E(n)}^{(k)} G_{(n)} + \mu Y^{(k)} - E^{(k)}(n), \]

where $T_{n,\mu} N W_{E(n)}^{(k)}(\cdot) := \text{fold}_n(T_{n,\mu} N W_{E(n)}^{(k)}(\cdot))$.
4: NST on the the tensor $G + \mu Y^{(k)} - X^{(k+1)}$.
5: $E^{(k+1)} \leftarrow S_{\mu} W^{(k)}(G + \mu Y^{(k)} - X^{(k+1)})$.
6: Updating weights:
\[ W_{E, n}^{(k+1)} \leftarrow \frac{1}{\sigma \epsilon_{E^{(k+1)}} + \epsilon_E}, \quad W_{E}^{(k+1)} \leftarrow \frac{1}{|\epsilon_{E^{(k+1)}} + \epsilon_E|}, \]
7: if convergence then
8: break
9: end if
10: end for

Output: $(\hat{X}, \hat{E})$

IV. EXPERIMENTAL RESULTS

A. Simulations

We simulated two multipass InSAR phase stacks of $128 \times 128$ pixels by 25 images with different spatial patterns. The corresponding linear deformation and elevation maps are shown in Figure 10. Note that the two geophysical maps of Simulation 1 are spatially uncorrelated, while those of Simulation 2 are highly correlated. Their linear deformation rates both range from $-15$[mm/year] to $15$[mm/year] and elevation values are from $-50$[m] to $50$[m]. The spatial baseline and the temporal baseline were chosen to be comparable to those of TerraSAR-X. Uncorrelated complex circular Gaussian noise was added to the two simulated stacks with an SNR of 5dB, i.e., according to PS model. To simulate sparse outliers in the stacks, 30% of pixels randomly selected from the phase tensor were replaced with uniformly distributed phases.

For visualizing the performance of the proposed method, we chose one interferogram from the recovered phase tensor $\hat{X}$ and visually compared it with those obtained by NL-InSAR [37] and HoRPCA [1] in Figure 7. Since NL-InSAR is designed for denoising one interferogram, whereas the others make use of the full image stack, to achieve a relatively fair comparison, the NL-InSAR result was obtained by averaging the results from 25 simulations of InSAR phase stacks. In our method, the spatial size of the tensor is set as $128 \times 128$ (i.e., the whole stack as one tensor), $\gamma$ is set to be $4.4 \times 10^{-4}$ and $\mu$ is kept constant at the value $10 \times \text{std}(\text{vec}(G))$. The experiments for the associated parameter setting will be introduced in the following section. The search window size and the patch size in NL-InSAR is $21 \times 21$ and $5 \times 5$, respectively. In addition, the phase profile marked by the short yellow line segment in Figure 7 are plotted in Figure 8. For a quantitative evaluation, we list the MSE values of the real-valued residual phases between the recovered phase tensor and the ground truth, i.e., $\text{MSE}(\angle(X - \text{conj}(\hat{X})))$, in cases of 30%, 40% and 50% percentages of outliers in Table II.

Furthermore, we compared the estimated results of geophysical parameters by PSI and the proposed RoMIO + PSI, using the simulated data. The outlier percentage was set to 30% and SNR was 5dB. $\alpha$ was set to $5 \times 10^{-3}$. The results are illustrated in Figure 11. The first two rows are the estimates of linear deformation rates of the two simulations and the last two rows are the corresponding elevation estimates. In addition to the experiments based on the full stack of 25 SAR images, experiments using only 9 images were conducted in order to test the RoMIO’s capability to handle small stacks. For the associated quantitative evaluation, we calculated both bias and standard deviation (SD) of the results and present them in Table III. To study the minimum number of images for RoMIO to achieve a reliable estimation, we plot the SD of the deformation estimates obtained by RoMIO + PSI w.r.t. a decreasing number of SAR images down to 7.

B. Real data

1) Berlin bridge: The first TerraSAR-X test area is a bridge in Berlin which is marked by the yellow rectangle shown in Figure 12 (Left), where the reference point for the elevation and seasonal motion is plotted red. To its right, the corresponding orthorectified optical image [61] and a streetview image from Google StreetView are also displayed. The InSAR stack contains over a hundred images. However, in order to test the performance under low number of images, 20 and 9 SAR images were selected from the full stack, respectively. They were selected to be similar in their distributions and spans of the temporal and spatial baselines, so that the Cramér-Rao bounds of the estimates are comparable. The baselines were also chosen to be close to uniform distribution. The 2D baseline distribution of the selected images can be seen in Figure 13. The estimated amplitudes of the seasonal motion and the elevation by PSI and RoMIO + PSI are demonstrated in Figure 15.

2) Las Vegas convention center: Another TerraSAR-X test dataset is the Las Vegas convention center, as shown in Figure 17. The total number of SAR images is 29. Since the building structure is complex and its spatial area is relatively large ($800 \times 850$ pixels), we separately processed the four parts of the whole InSAR phase stack as cropped with the red dashed rectangles shown in Figure 17 (Left). To its right, we also provide the associated optical image.
Ground truth
Corrupted Interferogram
NL-InSAR
HoRPCA
RoMIO
Simulation 1
Simulation 2
Fig. 7. Plots of one interferogram in the two simulated InSAR phase stacks, generated by the corresponding geophysical parameters shown in Figure 10, as well as the corrupted phases with an SNR of 5dB and 30% outliers, and the recovered results by three methods. Although the NL-InSAR result can maintain the smooth fringes very well, the edges of rectangle in the middle are more blurred compared to the other two results. This can be clearly observed at the two cropped parts in Figure 8. Compared to HoRPCA, the proposed method can better keep the original structure of the interferogram, since it can better capture the low rank structure of the data and model the sparse outliers by enhancing the low rank and the sparsity.

TABLE II
MSE PERFORMANCES OF NL-IN SAR, HoRPCA AND RoMIO ON THE SIMULATIONS SHOWN IN Figure 7

| Mean Square Error (MSE) [rad^2] | Simulation 1 | Simulation 2 |
|--------------------------------|--------------|--------------|
| 30% outliers                   | 0.03         | 0.04         |
| 40% outliers                   | 0.05         | 0.07         |
| 50% outliers                   | 0.12         | 0.12         |

TABLE III
QUANTITATIVE STUDY OF THE RESULTS IN Figure 10

| Simulation 1 | Deformation [mm/year] | Elevation [m] |
|--------------|-----------------------|---------------|
|              | SD        | bias       | SD      | bias       |
| PSI (25 images) | 2.08       | 0.01       | 8.18    | 0.42       |
| RoMIO+PSI (25 images) | 0.27       | 0.01       | 0.39    | 0.00       |
| RoMIO+PSI (9 images) | 0.29       | 0.02       | 1.59    | 0.01       |
| PSI (25 images) | 2.76       | 0.02       | 7.27    | 0.07       |
| PSI (9 images) | 9.16       | 0.05       | 21.12   | 0.21       |
| RoMIO+PSI (25 images) | 0.31       | 0.01       | 0.98    | 0.02       |
| RoMIO+PSI (9 images) | 0.31       | 0.01       | 1.17    | 0.13       |

TABLE IV
LAMPPPOST HEIGHT ESTIMATIONS OF THE TWO METHODS WITH 20 SAR IMAGES, ALONG WITH THE REFERENCE OF LiDAR POINT CLOUD.

| Unit (m) | Lamppost1 | Lamppost2 | Lamppost3 | Lamppost4 |
|----------|------------|------------|------------|------------|
| LiDAR height |           |            |            |            |
| PSI mean | 6.76       | 7.70       | 8.82       | 10.03      |
| PSI SD   | 1.39       | 2.17       | 0.36       | 2.96       |
| RoMIO+PSI mean | 7.15       | 7.09       | 8.91       | 8.01       |
| RoMIO+PSI SD | 1.30       | 1.74       | 0.28       | 0.46       |
from Google Earth. Similar to the previous experiment, we estimate the geophysical parameters by PSI and by the proposed method with a substack (9 SAR images), which were selected according to the same baseline criteria described in the previous paragraph. In Figure 18, the 2D distribution of spatial and temporal baselines of the total 29 measurements is demonstrated, along with those of the selected 9 measurements for reconstruction. The results are shown in Figure 20. Besides, we manually added 50% outliers to the stack and demonstrate the parameters retrieved by PSI and RoMIO + PSI with 29 SAR images in Figure 21.

V. DISCUSSIONS

A. Performance in simulations

According to the results shown in Figure 7, although the NL-InSAR result can maintain the smooth fringe very well, the edges of the rectangle in the middle are more blurred compared to the other two results. This can be clearly observed by the plots in Figure 8. Compared to HoRPCA, the proposed method can better keep the original structure of the interferogram, since it can better capture the low rank structure of the data and model the sparse outliers by enhancing the low rank and the sparsity. Consistently, the evaluation in Table II shows that under 30% percentage of outliers, both NL-InSAR and RoMIO can achieve reliable results. However, when the data is severely corrupted by outliers, e.g. 50% outliers, RoMIO can achieve a more robust performance than NL-InSAR.

Combining multipass InSAR techniques, e.g. PSI, with RoMIO can greatly improve the accuracy of parameter estimates. As illustrated in Figure 10, the results of PSI contain outliers. This is especially true for the result from a subset of the stack. The reason is that the periodogram used PSI is only asymptotically optimal, which means large bias is very likely to occur at low number of images. In contrast, the proposed method can robustly recover the parameters both using the full stack and using a subset of the stack. That is to say the proposed method can in turn effectively reduce the number of images required for a reliable estimation. For the quantitative performance, as illustrated in Table III, we can see the proposed geophysical parameter retrieval method — RoMIO + PSI — can improve the accuracy by a factor of ten to thirty comparing to PSI. This is also transferable to real data, as the simulation closely resembles real TerraSAR-X data. However, some artifacts are observed in the middle of the deformation estimates, which may be caused by choosing a large patch size (128 × 128) for optimization. Since the spatial information of phase tensors is utilized in the proposed approach, we found that with large patch sizes, over-smoothing artifacts may exist, especially in geometrically complex areas.

As shown in Figure 11, according to the results of the deformation reconstruction with decreasing numbers of SAR images, the proposed method can achieve a SD around 0.3[mm/year], which can improve the estimation accuracy of PSI more than ten times.

Figure 11 shows the accuracy of RoMIO + PSI can maintain at a better and more constant level compared to the PSI whose efficiency decreases linearly w.r.t. the number of images. At the number of images down to 7, the accuracy of RoMIO + PSI still keeps at a sub millimeter range which is about 30 times better than PSI. This creates an opportunity of multipass InSAR geophysical parameter reconstruction using very small stacks.

B. Parameter selection

The two parameters of RoMIO are µ and γ, where µ comes with the introduced Lagrange multiplier term, and γ controls...
the balance between the low rank tensor $X$ and the outlier tensor $\mathcal{E}$. As introduced in [51], we can keep $\mu$ constant with the value $10 \times \text{std}(\text{vec}(\mathcal{G}))$. For tuning $\gamma$, we first rewrite $\gamma = \alpha \times \lambda_n$, where a good choice for $\lambda_n$ can be set as $\frac{1}{\sqrt{\max(I_1, I_2, \ldots, I_N)}}$ according to [48], [51], and $\alpha$ is a factor for tuning. To show the influence of $\alpha$, Figure 9 presents MSE values of the real-valued residual phases of the phase stack recovered by RoMIO with respect to $\alpha$ (from $0.5 \times 10^{-3}$ to $1 \times 10^{-2}$), under different percentages of outliers. As shown in the plot, even under a high percentage of outliers, e.g. 30%, the operable range of $\alpha$ still keeps relatively wide. Of course, this range decreases as the percentage of outliers increases. Still, the parameter can be tuned using the L-curve method [11]. For a particular dataset, the optimal $\alpha$ for different percentages of outliers is similar (around $5 \times 10^{-3}$ in our simulation), which means that no assumptions about the amount of outliers is required.

C. Performance in real data

As shown in Figure 15, consistent with the simulations, the proposed method can achieve a more robust estimation result than the classical PSI. In particular, in case of limited number of images, the interpretation of the parameters retrieved by PSI is severely influenced by outliers. The results of the proposed method are more interpretable. One can observe that the amplitudes of the motion tend to increase from one side to the other. One plausible reason is that the deformation allowances on the two sides of the bridge are different. To verify this, a very high resolution image of the bridge is shown in Figure 12 (Middle). The yellow ellipses in the image show that there exists certain mechanical clearance between the bridge body and the road it attaches to. Interesting to note is that in the elevation maps in Figure 15 there are four elevated regions which correspond to the four lampposts on the bridge. We plot the corresponding profiles of height estimates from the results of PSI and RoMIO + PSI in Figure 14. Obviously, the four
The proposed method can achieve a SD around 0.3 mm/year, which can improve the estimation accuracy of PSI more than ten times. It shows the accuracy of RoMIO + PSI can maintain at a better and more constant level compared to the PSI whose efficiency decreases linearly w.r.t. the number of images. At the number of images down to 7, the accuracy of RoMIO + PSI still keeps at a sub millimeter range which is about 30 times better than PSI. This creates an opportunity of multipass InSAR geophysical parameter reconstruction using very small stacks.

In the results of Las Vegas convention center shown in Figure 20, the proposed method can mitigate the incorrectly estimated geophysical parameters much better than PSI, under limited SAR images. Besides, it is worth noting that the geometric structure of the object can be well preserved. For instance, as shown in Figure 19, we plot the elevation profiles indicated by the yellow arrows from the two results in Figure 20. The proposed method can preserve resolution by displaying a more obvious elevation step jumping than PSI, and simultaneously mitigates outliers. Moreover, when we synthetically corrupt the data by 50% of outliers, the geometric structures of the building cannot be well interpreted by the results of PSI as shown in Figure 21. In contrast, the proposed method can achieve much more reliable results.

VI. CONCLUSION

This paper studied the low rank property of object-based InSAR phase stacks and proposed Robust Multipass InSAR technique via Object-based low rank tensor decomposition (RoMIO). RoMIO can be combined with conventional multipass InSAR techniques to improve the estimation accuracy of geophysical parameters. Taking PSI as an example, the paper demonstrated that in typical condition of very high resolution spaceborne InSAR data, e.g. object size of 10 m, 5 dB SNR and 10 – 20 SAR images, the proposed approach can improve the estimation accuracy of geophysical parameters by a factor of ten to thirty, especially in the presence of outliers. These merits can in turn efficiently reduce the number of SAR images for a reliable estimation.

Based on our experiments, we can see that the spatial sizes of tensors can influence the efficiency of the proposed method. On one hand, with large spatial sizes, the low rank property of the phase tensor is generally more prominent, which gives a wide operable range of the regularization parameters in the optimization. But, over-smoothing artifacts may exist, especially in some geometrically complex areas. On the other hand, with small spatial sizes, although it can be a benefit for preserving small detail, the regularization parameters must be carefully tuned. Otherwise, the reconstructed phase tensor may have the risk to be turned into a rank-1 tensor. Therefore, the tensor size should be large enough to promote low-rankness of the true phase and the sparsity of outliers, but small enough to exclude complicated structures. According to the experiments in the paper, the typical patch size we utilized is around 100 × 100 pixels, and this can be improved by exploiting adaptive window.

Besides, the proposed approach is suitable for operational processing, as the only parameter that needs to be tuned, i.e. α, was shown to usually lie in the range from 1 × 10^{-3} to 1 × 10^{-1} based on both the simulated and real data experiments. Besides, the approach can easily be parallelized by carrying it out patch-wisely.

Currently, this approach relies on the segmentation of objects. For future work, we would like to investigate lower level geometric information in SAR images to relax the requirement of object masks. Furthermore, we are also planning to research objects in non-urban areas, where few of them present regular shapes, and attempt to investigate their inherent property which can be utilized for the improvement of geophysical parameter retrieval, based on the geometric information.

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Fig. 12. (Left) The TerraSAR-X test image of one bridge area in Berlin as cropped by the yellow rectangle. The red point is the reference point for the elevation and seasonal motion reconstruction in this area. (Middle) The associated orthorectified optical image, generated using semi-global matching [61]. (Right) The streetview image from Google StreetView.

Fig. 13. The 2D distribution of spatial and temporal baselines of the selected 20 and 9 measurements for reconstruction. The baselines were also chosen to be close to uniform distribution.

Fig. 14. The extracted two profiles of height estimates located at the yellow arrow positions of the results of PSI and RoMIO + PSI, along with the lamppost height profile of LiDAR. Obviously, the four lampposts (shown by the black dash ellipses) are well distinguishable in the result of the proposed method.

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PSI with 20 SAR images  PSI with 9 SAR images  RoMIO + PSI with 20 SAR images  RoMIO + PSI with 9 SAR images

Amplitudes of seasonal motion

Elevation

Fig. 15. Geophysical parameter estimations (amplitudes of the seasonal motion and elevations) of the area by PSI and RoMIO + PSI with 20 and 9 SAR images. Consistent with the simulations, the proposed method can achieve a more robust estimation result than the classical PSI. In particular, under limited number of images, the interpretation of the parameters retrieved by PSI is severely influenced by outliers. The results of the proposed method are more interpretable. One can observe that the amplitudes of the motion tend to increase from one side to the other. One plausible reason is that the deformation allowances on the two sides of the bridge are different. To verify this, a very high resolution image of the bridge is shown in Figure 15 (Middle). Interesting to note is that there are four elevated regions which correspond to the four lampposts on the bridge. We plot the corresponding two profiles from the results of PSI and RoMIO + PSI in Figure 14.

Fig. 16. LiDAR point cloud of the study Berlin bridge

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Fig. 17. (Left) The TerraSAR-X test image of the Las Vegas convention center. Since the building structure is complex and its spatial area is large (800 × 850 pixels), we separately process the four parts of the whole InSAR phase stack as cropped with the red dashed rectangles in the figure. (Right) The associated optical image from Google Earth.

Fig. 18. The 2D distribution of spatial and temporal baselines of the total 29 measurements is demonstrated, along with those of the selected 9 measurements for reconstruction. The baselines were also chosen to be close to uniform distribution.

Fig. 19. The estimated elevation profiles of the two methods, which are selected by the yellow arrows in Figure 20. The proposed method can preserve resolution by demonstrating a more obvious elevation step jumping than PSI, and simultaneously mitigate incorrectly estimated points.

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