Optimal DG location and sizing for minimum active power loss in radial distribution system using firefly algorithm

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Abstract – In this paper, a novel optimization algorithm is presented for the optimal location and sizing of Distributed Generation (DG) units on distribution systems. For this purpose, a recently based meta-heuristic called Firefly Algorithm (FA) has been employed to minimize the total active power losses. The results show considerably improved in voltage profiles of all the buses and enhance the voltage stability index. The investigations were tested on IEEE 33 bus radial distribution system. Simulation results demonstrate the effectiveness of firefly algorithm. Comparison with another method is also given.

Keywords: Generation, Firefly Algorithm, Active Power Losses, Radial Distribution Network

I. Introduction
Distributed or dispersed generation (DG) is used in order to produce electrical power for a small-scale (1 kW to 50 MW) that is usually connected to or embedded in the distribution system [1]. The advantage of DG are numerous [2, 4] and the reasons for implementing DG units are an energy efficiency or rational use of energy, diversification of energy resources, reduction of on-peak operating cost, deferral of network upgrades, minimizing power losses, lower transmission and distribution costs, and possible increase of service quality to the end-customer. Moreover, DGs are available in modular units, characterized by ease of finding sites for smaller generators, shorter construction times, lower capital costs and reduction of gaseous emissions.

In literature different analytical and meta-heuristic optimization based algorithms have been proposed for optimum DG location and sizing. In [5], the authors in [6] have employed an analytical approach for the optimum DG unit location with fitness function of minimization of active power losses. Further, the authors in [7] have developed a new analytical method for the voltage profile enhancement and compensation of active power losses. The authors in [8] have proposed a meta-heuristic technique called Ant Bee Colony (ABT) algorithm for reducing the active power losses in distribution power system. Also, the authors in [9] and [10] have applied a Cuckoo Search Algorithm (CSA) for DG placement and sizing problem in order to reduce the active power loss and to enhance the network voltage profile. In [11], the authors have proposed particle swarm optimization (PSO) algorithm for reducing the power losses in the distribution system. Furthermore, the authors in [12] have proposed on the installation of the capacitor bank with objective function of minimization of total power losses and net saving maximization using a novel optimization algorithm. Other prepositions in [13] based on multi-objective optimization problem for improving the transient stability using a hybrid evolutionary algorithm.

The present study describes the employment of a novel meta-heuristic called Firefly Algorithm (FA) for the optimal placement and sizing of DG unit in radial distribution networks. This problem is formulated as an optimization problem. The proposed algorithms have been tested on IEEE 33 bus radial distribution systems.

![Figure 1. Electrical equivalent of two node system.](image)
II. Problem formulation

A. Active power loss

In this study, the optimal siting and sizing of DG units in 33 bus radial distribution networks is formulated as an optimization problem to reduce the total active power losses. This latest can be calculated by Eq. 1. Figure 1 shows the electrical equivalent of radial distribution system.

From Figure 1, the following equation can be written:

\[ PL(i) = \eta \left( \frac{p_i^2 + q_i^2}{V_i^2} \right) \]  

(1)

Therefore, the objective function is calculated using the following equation:

\[ f = \sum_{i=1}^{N_{bus}} PL = \sum_{i=1}^{N_{bus}} PL(i) = \sum_{i=1}^{N_{bus}} \eta \left( \frac{p_i^2 + q_i^2}{V_i^2} \right) \]  

(2)

Where \( i \)-1 sending end node; \( i \) receiving end node; \( r_i + jx_i \) is the line impedance connected between \( i-1 \) and \( i \); \( I_i \) current of branch \( j \); \( V_{i,j} \) voltage of node \( i-1 \); \( V_i \) voltage of node \( i \); \( P_i \) and \( Q_i \) active and reactive power load fed through node \( i \).

- **Total Loss reduction (TLR)**
  
  Total Loss Reduction (TLR) is calculated using Eq. (3) [14]:

\[ TLR\% = \frac{\sum_{i=1}^{N_{bus}} PL_{W/DG} - \sum_{i=1}^{N_{bus}} PL_{W/\text{DG}}}{\sum_{i=1}^{N_{bus}} PL_{W/\text{DG}}} \times 100 \]  

(3)

Where, \( PL_{W/DG} \) is the total line losses in the system with the employment of DG and \( PL_{W/\text{DG}} \) is the total line losses in the system without DG

III. Constraints

The objective function is subjected to main constraints in the optimization process in the proposed methodologies are:

- Power constraint
- Voltage constraint
- Active power losses constraint.
- DG size constraint.

B. **Power constraint**

The equality constraints are active/reactive power flow equations as:

\[ \begin{align*}
P_{Gi} - P_{Di} & = \sum_{j=1}^{N_{bus}} V_j \cdot Y_{ij} \cdot \cos(\theta_{ij} + \delta_j - \delta_i) \\
Q_{Gi} - Q_{Di} & = \sum_{j=1}^{N_{bus}} V_j \cdot Y_{ij} \cdot \sin(\theta_{ij} + \delta_j - \delta_i)
\end{align*} \]  

(4)

Where \( P_{Gi} \) and \( Q_{Gi} \) are the active (resp. reactive) power generated at the \( i \)-th bus; \( P_{Di} \) and \( Q_{Di} \) are the active (resp. reactive) load demand at the same bus; \( Y_{ij} \) and \( \delta_i \) are the admittance magnitude (resp. angle) of branch connecting bus \( i \) and \( j \).

C. **Voltage constraint**

The voltage magnitude must keep within the specified limits at each bus [15]:

\[ V_{min} \leq V_i \leq V_{max} \]  

(5)

Where \( V_{min} \) and \( V_{max} \) are the lower and upper limits of bus voltage, respectively.

D. **Active power losses constraint**

The losses after installing DG in power grid should be less than or equal losses before installing DG [15].

\[ PL \text{ with DG } \leq PL \text{ without DG} \]  

(6)

E. **Distributed generation size constraint**

To obtain a reasonable solution, the size of generator should not be so small or so high with respect to load value. The DG size is considered not less than zero and not more than the total active load demand as following [15]:

\[ 0 \leq \text{size of DG}(P_{DG}) \leq \sum_{i=1}^{N_{bus}} P_{Di} \]  

(7)

Where \( P_{Di} \) is the active load demand at the same bus.

IV. Proposed algorithm

Firefly Algorithm (FA) is invented by Xin-She Yang [15] for solving multimodal optimization problem. The development of FA is based on flashing behavior of fireflies. There are about two thousand firefly species where the flashes often unique for a particular species. The flashing light is produced by a process of bioluminescence where the exact functions of such signaling systems are still on debating. Nevertheless, two fundamental functions of such flashes are to attract mating partners (communication) and to attract potential prey.

For simplicity, the following three ideal rules are introduced in FA development [16]:

- all fireflies are unisex so that one firefly will be attracted to other fireflies regardless of their sex,
- attractiveness is proportional to their brightness, thus for any two flashing fireflies, the less brighter one will move towards the brighter one,
- The brightness of a firefly is affected by the landscape of the objective function.

For maximization problem, the brightness can simply be proportional to the value of the objective or fitness function.

V. Application of the Firefly Algorithm to the problem

In this section, Firefly Algorithm (FA) is proposed to discover the best placement and sizing of Distributed generation (DG) unit in a radial distribution system to
minimize the total active power loss in the system. By reducing power loss, the voltage profile at each bus is also expected to be improved the voltage profiles and increased values of voltage stability index. Figure 2 presents the general flowchart of Firefly algorithm for evaluating the objective function.

![Flowchart](image)

**VI. Results and discussion**

In this study, the proposed algorithms are used to determine the optimal location and size of the DG unit and they have been carried out on IEEE 33-bus radial distribution system. The FA properties in this simulation are set as follows:

| Setting                  | Value |
|--------------------------|-------|
| Number of iteration      | 50    |
| Number of population     | 20    |
| Variation of attractiveness | 0.5  |
| Randomization            | 0.8   |
| Absorption coefficient   | 1     |

**IEEE 33-bus Radial Distribution System**

The test system is IEEE 33-bus radial distribution system, with the total load is 3.715 MW and 2.3 MVar, its voltage level is 12.66 kV, this system contains 33 bus and 32 branches. Its corresponding scheme is presented in Figure 3 [17].

![IEEE 33-Bus radial distribution system](image)

**F. Results**

The DG unit localization, corresponding sizes and active power losses in the cases without and with DG unit using the proposed algorithm and PSO algorithm find by [11] are respectively summarized in TABLE II. The voltage profile, minimum and maximum voltage, voltage stability index, minimum and maximum voltage stability index and the active power losses are presented in Figures. (4-8) simultaneously.

| IEEE 33-Bus Test System | Without DG | With DG | PSO [11] | Proposed Method |
|-------------------------|------------|--------|----------|-----------------|
| Optimum location        | -          | 7      | 6        |
| Optimum DG size (MWA)   | -          | 2.91   | 2.60     |
| Active Power Losses (KW)| 211.00     | 115.1  | 111      |
| Loss reduction %        | -          | 45.45  | 47.39    |

**G. Discussion**

The effect of DG placement is also measured by calculating the active power loss, the voltage profiles and
the voltage stability index. Table III shows the effect of DG placement on system performance. From these results, we can observe the advantage of DG units in improvement of system performances, as reduction of total system losses and the voltage index stability enhancement. In order to validate the performance of the proposed algorithm in this study, we have used IEEE 33-bus test distribution system.

When the proposed method is applied on test system, it was found that the proposed method gives much better voltage profile as compared to the base case. Fig. 4 shows voltage profile of IEEE 33-bus test distribution system (with and without DG placement). From Fig. 5, it can be observed that the minimum voltage is raised from 0.90 pu in the case without DG unit to 0.94 pu in the case with DG unit using the proposed method.

Fig. 6 shows the voltage stability indices of test system. The weakness of voltage stability indices for all buses in the distribution system before integration DG unit is obvious. But after integration DG unit, the buses stability indexes are considerably enhanced. Fig. 7 shows the minimum and maximum voltage stability index of the test system (with and without DG placement).

The proposed method also results in total power loss reduction. TABLE II shows the effect of DG placement on loss reduction, using the proposed and another existing method. From TABLE II, it can be observed after installation of DG units, the active power losses have been significantly reduced. The proposed algorithm is found better in performance than PSO algorithm. Where the proposed algorithm gives 2% more power loss than PSO algorithm. Fig. 8 shows the active power loss at buses with and without DG for IEEE 33 bus test system.
VII. Conclusion

In this paper, the problem of optimal DG unit placement and sizing in radial distributed network has been treated. For this reason, a recent Meta-heuristic technique known as firefly Algorithm is employed to minimize the total active power losses. Its effectiveness and robustness is compared to the particle swarm optimization algorithm. Simulations were performed on IEEE 33 bus radial system. The obtained results clearly reveal the effectiveness of the proposed algorithm in total active power losses minimizing compared to PSO algorithm.

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