Stabilization of golden cages by encapsulation of a single transition metal atom

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Golden cage-doped nanoclusters have attracted great attention in the past decade due to their remarkable electronic, optical and catalytic properties. However, the structures of large golden cage doped with Mo and Tc are still not well known because of the challenges in global structural searches. Here, we report anionic and neutral golden cage doped with a transition metal atom MAu16 (M = Mo and Tc) using Saunders ‘Kick’ stochastic automation search method associated with density-functional theory (DFT) calculation (SK-DFT). The geometric structures and electronic properties of the doped clusters, MAu16q (M = Mo and Tc; q = 0 and −1), are investigated by means of DFT theoretical calculations. Our calculations confirm that the 4d transition metals Mo and Tc can be stably encapsulated in the Au16− cage, forming three different configurations, i.e. endohedral cages, planar structures and exohedral derivatives. The ground-state structures of endohedral cages C2v Mo@Au16−(a) and C1 Tc@Au16−(b) exhibit a marked stability, as judged by their high binding energy per atom (greater than 2.46 eV), doping energy (0.29 eV) as well as a large HOMO–LUMO gap (greater than 0.40 eV). The predicted photoelectron spectra should aid in future experimental characterization of MAu16− (M = Mo and Tc).

1. Introduction

Nanoclusters display many new properties, which are usually not found in their bulk counterparts [1–3]. These novel properties can be attributed almost to strong relativistic effects and finite-size quantum effects [4,5]. Gold clusters, in particular, have received special attention due to their potential technological applications as in the fabrication of materials in catalysis [6–11], chemical/biological sensors [12], medical sciences [13] and so forth. As the geometry of the cluster is closely related to its properties, an understanding of the cluster geometry is of primary interest. It is very important to identify their geometric structures...
for the controlled use of clusters in future nanotechnology. In the past couple of decades, both gold clusters and gold cluster doping with impurity atoms of alkali metal or transition metal have attracted the attention of theoreticians and experimentalists working in the field of cluster science [14–26]. The results of the previous investigations indicate that the introduction of a transition metal dopant atom in the gold cluster can change its structure and electromagnetic properties significantly [22–24]. In particular, photoelectron spectroscopy (PES) in combination with density-functional theory (DFT) calculations [27] revealed that the ground-state structure of the Au16 cluster anion has a highly stable hollow cage with a large intermolecular volume similar to that of fullerences [28]. This feature leads to the possibility of forming a new class of golden cages with particular properties by endohedral doping similar to those of the endohedral fullerenes. Subsequently, the investigation of doping one guest atom into the Au16− cage has prompted immediate extensive interest by both theoreticians and experimentalists with the purpose to design novel endohedral gold-caged clusters, as the chemical and physical versatility can be exploited by tuning the structural and electronic properties of gold clusters [29–34]. The most recent ab initio calculations showed the gold-covered bimetallic clusters M@Au16 (n = 8–17) with closed-shell structures obeying the 18-electron rule and starting from n = 9 the doped-metal atom prefers to be entirely covered by pure gold atoms to form the lowest energy structure [29]. Subsequently, a series of doped gold anion clusters MAu16− (Ag, Zn, In and Cu) have been systematically studied using PES experiment and theoretical calculations by Wang et al. [18,19]. It is found that Ag, Zn and In can all be doped inside the Au16− cage with little structural distortion. Similar to Cu, they transfer their valence electrons to the golden cage and form endohedral charge transfer complexes. However, in contrast to a previous theoretical prediction on MAu16− (Ag, Zn, In and Cu), the doping Au16− cluster with a Si, Ge or Sn atom led to completely different structures, forming exohedral structure where the tetrahedral golden cage is completely distorted due to the strong M–Au local interactions [30]. Many physical chemists have made many efforts to deal with the global optimization of clusters using automated procedures [35–38]. For example, Car & Parrinello’s [35] well-known ‘dynamic simulated annealing’ combines molecular dynamics (MD) and DFT. Shayegehi et al. [36] present an approach for the global optimization of monoatomic or binary clusters. Very recently, a global optimization technique, using neural network potentials combined with the basin-hopping method, to study medium-sized metal clusters was proposed by Jiang et al. [39,40].

Up to now, Au16 cluster and golden cage Au16 doping with impurity atoms of 3d transition metal and alkali metal have attracted the attention of researchers in both theoretical and experimental studies devoting themselves to working in cluster science [16,18–23]. In a recent study, we have provided the first theoretical evidence of endohedral doping of the golden cages by the early 4d transition metals Y, Zr and Nb in Au16− cage [24]. The closeness of the vertical/adiabatic detachment energy (ADE) for doped clusters MAu16− (3.506/3.632 eV for Y-doped, 2.693/2.837 eV for Zr-doped and 3.406/3.496 eV for Nb-doped) reveals a negligible geometry change between the anionic and neutral species. However, to the best of our knowledge, only a limited literature existed on the 4d transition metal impurity atoms as dopants in golden cage Au16 clusters, there are still many open questions for 4d transition metal atoms, Mo, Tc and so forth. For example, there is still no experimental evidence for verifying the predicted structures directly. What are equilibrium structures and relative energies for doped golden cage Au16 clusters? Are there preferred endohedral or exohedral doping nanostructures and how are these geometric structures formed? The large empty space inside the Au16 cluster anion cage allows for possible endohedral doping to form a new class of endohedral golden cages. The endohedral golden cages could display new chemical physical and catalytic properties which are different from those of the bare golden cage clusters. Thus, an accurate first-principles calculation based on the density-functional theory is fundamental to understand the structural and electronic properties of those clusters. Furthermore, most previous theoretical calculations on atomic clusters were building structures manually as well as the presumed symmetric constraints. An unconstrained global search on the cluster potential energy surface is needed.

In the present work, we report a theoretical study of doping a 4d transition metal atom M (M = Mo and Tc) into the Au16 cage cluster. A number of anionic and neutral doped golden cage isomers are obtained using Saunders ‘Kick’ global search technique [41] combined with DFT calculation (SK-DFT). Recently, we have successfully employed the SK-DFT method for global minimum searches of relatively small clusters, and provided a comprehensive analysis of the ability of current methods to determine the geometry of the ground state of clusters [42–46]. The specific objectives of this work are fourfold: (1) to identify structures of the lowest-energy/low-lying clusters using a global optimization method coupled with DFT calculation; (2) to provide useful information for MAu16 cluster systems in future photoelectron spectroscopy experiment; (3) to compare the results of our extensive computations.
performed using SK-DFT with previously experimental findings on the host golden cage and some other 3d and early 4d transition metal atoms-doped gold clusters; (4) to characterize the stability of the lowest-energy clusters by computing their binding energy per atom, doping energy and the highest occupied and lowest unoccupied molecular orbit (HOMO–LUMO) gap. At this stage, although other energetically more favourable structures could not be ruled out strictly, we believe that the lowest-energy structures of MAu16q found here are at least powerful candidates for their ground states, which are hoped to be verified in the future photoelectron spectroscopy experiments and calculations at more accurate levels of theory. This work should be interesting for future material physicists and chemists, especially those designing new materials.

2. Computational methods

The structure prediction of MAu16q (M = Mo and Tc; q = 0, –1) clusters is based on the Saunders ‘Kick’ stochastic automation search method [41] combined with density-functional theory calculation (SK-DFT) which has been successfully applied in the structural prediction of a number of cluster systems [22–24,42–46]. All the mixed atoms, including 16 gold atoms and a single transition metal atom (Mo and Tc), are placed at the same point initially and then are ‘kicked’ randomly within a size-controlled hollow sphere with a radius \( R \) for avoiding biasing search. The kick size (radius \( R \)) in the hollow sphere is 15 Å in this work. The kick method runs at the PBEPBE/LANL2DZ (‘PBEPBE’ functional [47] with a scalar relativistic effective core potential (RECP) and LANL2DZ basis set [48]) level up to 800 times until no new minima appeared. Afterwards, the top several isomers approximately 0.3 eV from each minimum at the PBEPBE/LANL2DZ level were all regarded as potential candidate lowest-energy structures to be further reoptimized and evaluated with the larger basis set. As no symmetry constraints are imposed, the geometries obtained should correspond to minima. The reoptimization and evaluation used PBEPBE exchange-correlation functional with the large basis set Au/SDD+2f/M/ECP28MBW, followed by vibrational frequency calculations. Here, ‘SDD+2f’ denotes the Stuttgart/Dresden RECP valence basis [49,50] augmented by two sets of \( f \) polarization functions (exponents = 1.425, 0.468) for Au, and ‘ECP28MBW’ denotes the Stuttgart contracted pseudo-potential basis set for 4d transition metal atom M (M = Mo and Tc) [51,52]. All calculations were performed using the Gaussian 09 package [53].

The accuracy of PBEPBE/Au/SDD+2f/M/ECP28MBW level of theory was validated using five exchange-correlation functionals (PBEPBE [47], B3LYP [54], BP86 [55,56], PW91 [57] and TPSS [58]) with the same RECP valence basis SDD+2f on pure gold clusters Au16q (q = 0, –1). The first ADE and vertical detachment energy (VDE) are calculated and photoelectron spectra are also simulated. Furthermore, to quantitatively compare simulated spectrum with the experimental spectrum [18,27], we calculate the root-mean-square deviation (RMSD) for the labelled peaks \( X \sim C \) [18]. Comparing the calculated first ADE/VDE, RMSD and simulated photoelectron spectra with measured results by PES experiment for the Au16q−, PBEPBE/SDD+2f level of theory gives very good agreement with the experimental observations (table 1 and figure 1), and, therefore, the same level has been selected as the method of choice for MAu16q (Mo and Tc; q = 0, –1) species also. Here, the first ADE is determined by calculating the energy difference between the optimized anion geometry and the optimized neutral geometry. The first VDE is defined as the energy difference between the neutral clusters at optimized anion geometry clusters and optimized anion clusters. Then, the first VDE is added to the orbital energies of the deeper occupied orbitals to obtain VDEs of the higher detachment channels. The VDEs so obtained are fitted with a full width at half-maximum (FWHM) of 0.09 eV to yield the simulated spectra, which are used to compare with the experimental spectra. This method has been used successfully in a number of previous studies and has been shown to yield VDEs in good agreement with experimental photoelectron spectra [59–64].

3. Results and discussion

Two important types of structures A/B, simulated photoelectron spectra of Au16− for structures A/B using five different functionals (B3LYP, BP86, PBE, PW91 and TPSS) in comparison with experimental photoelectron spectra [27] for host gold cluster Au16− are shown in figure 1. Table 1 gives various structural and energetic characteristics of the top-two structures of host pure neutral and anionic Au16 clusters, including the spin multiplicity (SM), symmetry type (Sym), total energy (\( E_t \)), the relative energy (\( \Delta E \)), calculated/experimental first ADE/VDE and RMSD. The top-11 lowest-energy isomers of MAu16− (M = Mo and Tc) obtained from a SK global search combined with DFT optimization and total energy calculation at the PBEPBE/LANL2DZ and PBEPBE/Au/SDD+2f/M/ECP28MBW levels
are presented in figures 2 and 3 (the Cartesian coordinates of these low-lying isomers can be found in the electronic supplementary material). The energy values (in eV) given beneath each isomer are the relative energy with respect to the leading lowest-energy isomer. The energy values in the first line are based on the PBE/LANL2DZ level. The energy values in parentheses in blue are calculated at the PBE/PBE/Au/SDD+2f/M/ECP28MW level of theory. The simulated anion photoelectron spectra company with structures of the several candidate lowest-energy isomers (approx. 0.3 eV) of $\text{MAu}_{16}^-$ ($M = \text{Mo and Tc}$) are shown in figures 4 and 5. The spin multiplicity (SM), symmetry type (Sym), relative energy ($\Delta E$), binding energy (BE) per atom, doping energy (DE) per atom, HOMO–LUMO energy gap

Figure 1. Structures and simulated photoelectron spectra for the two low-lying isomers of $\text{Au}_{16}^-$ using five different methods. For comparison, the experimental spectra of $\text{Au}_{16}^-$ cage are shown by the black curves. The experimental PES spectra are cited from [27].
3.99 than those of structure B (ADE/VDE, theoretical: 3.89/4.02 eV for A, 3.75/3.78 eV for B; experimental: calculated first ADE and VDE of structure A are in accord with experimental PES data \[18,27\] and better agrees better than that of C

detachment energy (ADE/VDE, eV), and the RMSD (eV).

anionic structure A is 0.042 eV above the planar structure B at PBEPBE/SDD in figures 2 and 3 and also given in table 2.

PBEPBE/LANL2DZ level. To clearly compare simulated PES with the experimental PES, we present B3LYP, BP86, PBE and PW91, respectively, indicating that planar isomer is the most possible structure.

For the neutral and anionic host cluster Au\(_{16}\), we present two important types of structures: a perfect cage \(D_{2d}\) structure A and a high symmetric planar \(C_{2v}\) structure B. It is somewhat surprising that anionic structure A is 0.042 eV above the planar structure B at PBEPBE/SDD+2\(f\) level of theory; however, calculated first ADE and VDE of structure A are in accord with experimental PES data \[18,27\] and better than those of structure B (ADE/VDE, theoretical: 3.89/4.02 eV for A, 3.75/3.78 eV for B; experimental: 3.99 \(\pm\) 0.03/4.03 \(\pm\) 0.03 eV, table 1). Our recent study \[23\] found that the global minimum structure \(2v\) isomer B with the experimental spectrum (figure 1). These results lead us to conclude that the structure A should be a reasonable isomer in the Au\(_{16}\)\(^{-}\) gas cluster beam. For neutral Au\(_{16}\), isomer A is less stable than isomer B by 0.639, 0.352, 0.181 and 0.155 eV at four functionals B3LYP, BP86, PBE and PW91, respectively, indicating that planar isomer is the most possible structure.

### Table 1. Comparison of structural and energetic characteristics of structures A/B using different methods for pure neutral and anionic Au\(_{16}\).\(^{a}\)

| method | charge | SM | Sym | \(E_1\) | \(\Delta E\) | ADE | VDE | RMSD |
|--------|--------|----|-----|--------|-----------|------|------|------|
| B3LYP | –1     | 2  | \(D_{2d}\) | –2173.21564633 | 0.000 | 3.83 | 3.98 | 0.13 |
|        | 0      | 1  | \(C_2\)   | –2173.07498251 | 0.000 |
| BP86  | –1     | 2  | \(D_{2d}\) | –2174.86868788 | 0.000 | 4.05 | 4.18 | 0.23 |
|        | 0      | 1  | \(C_1\)   | –2174.71981703 | 0.000 |
| PBE   | –1     | 2  | \(D_{2d}\) | –2173.23223352 | 0.000 | 3.89 | 4.02 | 0.06 |
|        | 0      | 1  | \(D_{2d}\) | –2173.08939878 | 0.000 |
| PW91  | –1     | 2  | \(C_2\)   | –2174.2403705 | 0.000 | 3.96 | 4.10 | 0.19 |
|        | 0      | 1  | \(D_{2d}\) | –2174.09458239 | 0.000 |
| TPSS  | –1     | 2  | \(C_1\)   | –2172.1183722  | 0.000 | 3.65 | 3.86 | 0.20 |
|        | 0      | 1  | \(S_4\)   | –2171.9843657  | 0.000 |

| structure B |
|-------------|
| B3LYP       | –1     | 2  | \(C_{2v}\) | –2173.23596465 | –0.553 | 3.74 | 3.79 | 0.26 |
| BP86        | –1     | 2  | \(C_{2v}\) | –2174.87590664 | –0.196 | 3.89 | 3.93 | 0.25 |
| PBE         | –1     | 2  | \(C_{2v}\) | –2173.23739128 | –0.042 | 3.75 | 3.78 | 0.31 |
| PW91        | –1     | 2  | \(C_{2v}\) | –2174.24073219 | –0.011 | 3.82 | 3.86 | 0.28 |
| TPSS        | –1     | 2  | \(C_{2v}\) | –2172.10762424 | 0.291 | 3.62 | 3.65 | 0.39 |

| Expt. \(^{b}\) |
|----------------|
| 3.99 \(\pm\) 0.03 | 4.03 \(\pm\) 0.03 | 0.00 |

\(^{a}\)Shown are the spin multiplicity (SM), symmetry type (Sym), total energy \((E_1, \text{a.u.})\), the relative energy \((\Delta E, \text{eV})\), calculated first adiabatic/vertical detachment energy \((\text{ADE/VDE, eV})\), and the RMSD (eV).

\(^{b}\)References \[18\] and \[27\].

\((E_{\text{gap}})\), and calculated first ADE and VDE for the top five of M@Au\(_{16}\)\(^{-}\) (M = Mo and Tc) are shown in figures 2 and 3 and also given in table 2.

3.1. Geometric structure and stability

For the neutral and anionic host cluster Au\(_{16}\), we present two important types of structures: a perfect cage \(D_{2d}\) structure A and a high symmetric planar \(C_{2v}\) structure B. It is somewhat surprising that anionic structure A is 0.042 eV above the planar structure B at PBEPBE/SDD+2\(f\) level of theory; however, calculated first ADE and VDE of structure A are in accord with experimental PES data \[18,27\] and better than those of structure B (ADE/VDE, theoretical: 3.89/4.02 eV for A, 3.75/3.78 eV for B; experimental: 3.99 \(\pm\) 0.03/4.03 \(\pm\) 0.03 eV, table 1). Our recent study \[23\] found that the global minimum structure \(2v\) isomer B with the experimental spectrum (figure 1). These results lead us to conclude that the structure A should be a reasonable isomer in the Au\(_{16}\)\(^{-}\) gas cluster beam. For neutral Au\(_{16}\), isomer A is less stable than isomer B by 0.639, 0.352, 0.181 and 0.155 eV at four functionals B3LYP, BP86, PBE and PW91, respectively, indicating that planar isomer is the most possible structure.
Figure 2. The 11 lowest-energy isomers of MoAu16\(^{−}\) cluster obtained by SK-DFT. All the energy values (in eV) given beneath each isomer are the relative energy with respect to the leading lowest-energy isomer. The relative energies in the first line are based on the PBEPBE/LANL2DZ level. The energy values in parentheses are based on the PBEPBE/Au/SDD+2f/M/ECP28MWB level of theory.

In order to compare the degree of structural change of structure A under different point group symmetry, we calculate the average bond length. The results show that the average bond length of anionic Au\(_{16}\) is 2.85, 2.81, 2.80, 2.80, 2.78 Å for B3LYP, BP86, PBE, PW91, TPSS functional, respectively, and for neutral Au\(_{16}\), the calculated average length using the five functional is 2.86, 2.81, 2.81, 2.81, 2.79 Å. As can be seen, whether for neutral cluster or anionic Au\(_{16}\) cluster, the calculated values using BP86, PBE, PW91 and TPSS functionals are close to each other (about 2.80 Å for Au\(_{16}\) and 2.81 Å for Au\(_{16}^{−}\)), indicating that structure distortion of these isomers calculated using different functionals is not obvious. The result of B3LYP functional is a bit larger than those of other functionals. B3LYP functional is not suitable for
the study of gold clusters, which has been confirmed by the study in the pure golden clusters $\text{Au}_n^-$ ($n = 16–18$) [27].

One of the most important questions that we want to address here is to discover the lowest-energy structures of the $\text{MAu}_16^-$ clusters. We have obtained many isomers and determined the lowest-energy structures for $\text{MAu}_16^-$ ($\text{M} = \text{Mo}$ and $\text{Tc}$) using the computation scheme SK-DFT described in §2. The ground-state structures and some low-lying metastable isomers of $\text{MAu}_16$ cluster anions accompanied with relative energies are given in figures 2 and 3, where a blue sphere refers to the impurity atom $\text{M}$. All the low-lying isomers are formed in three different configurations, i.e. endohedral cages (isomers a–f), plane structures (isomers g–i) and exohedral derivatives (isomers j–k). For $\text{MoAu}_{16}^-$, all the 11

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**Figure 3.** The 11 lowest-energy isomers of $\text{TcAu}_{16}^-$ cluster obtained by SK-DFT. All the energy values (in eV) given beneath each isomer are the relative energy with respect to the leading lowest-energy isomer. The relative energies in the first line are based on the PBEPBE/LANL2DZ level. The energy values in parentheses are based on the PBEPBE/Au/SDD+2f/M/ECP28MWB level of theory.
Figure 4. Structure and simulated photoelectron spectrum from the lowest-energy isomer of Mo@Au$_{16}^-$. 

Figure 5. Structures, relative energies ($\Delta E$) in eV and simulated photoelectron spectra from the top-five lowest-energy isomers (approximately 0.3 eV) of Tc@Au$_{16}^-$. 

Lowest-energy isomers are found to prefer the lowest spin state. However, the stability of isomers of TcAu$_{16}^-$ cluster is lower along with the increase of the spin multiplicities. Specifically, multiplicities vary substantially in some cases (SM = 2 for MoAu$_{16}^-$-d, but 7 for TcAu$_{16}^-$-d, similar situations occur in
structures e–j). This may be attributed to the fact that the valence electron configuration of Mo is 4d^55s^1, the unpaired electron in the 5s orbital is easily hybridized with 4d ones to form 4d–5s hybridization, thus reducing spin multiplicity. For TcAu_{16}^–, the valence electron configuration of Tc is 4d^35s^2. 4d orbit is just a half-filled shell and two electrons fill the 5s orbit; because of this the electron structure is not easy to break, thereby making the isomer d of TcAu_{16}^– high spin. Our SK-DFT calculations show that the six candidate lowest-energy isomers for MAu_{16}^– are almost all low-symmetry ‘endohedral cages’ with a dopant atom trapping inside the cage. Exohedral and plane structures for MAu_{16}^– are obviously less stable than endohedral structures. As shown in figures 2 and 3, the top-six lowest-lying isomers of MoAu_{16}^– resemble closely the shape of TcAu_{16}^– clusters, although the order of total energies is completely dissimilar to each other. For the MoAu_{16}^– cluster, an endohedral structure (a) with relatively high symmetry (C_{2v}) was obtained, which can be derived from the previously discovered M@Au_{12}^– (M = W and Mo) icosahedral structure [65] with high symmetry and significant stability by capping four additional Au atoms on two triangular broadside faces. Other five endohedral isomers from MoAu_{16}^– (b) to MoAu_{16}^– (f) with low symmetry were less stable than the global minimum structures by 0.41–0.87 eV at high-level PBEPA/Au/SDD+2f/M/ECP28MWB. Considering the large relative energies for such isomers, we can rule out the possibility that these higher energy isomers become the ground-state structure. As for TcAu_{16}^– cluster, the global minimum structure (b) has a quintet state with low symmetry C_1. However, five structures (isomers a, b, c, d, f) are found to be close to each other in energy (approximately 0.3 eV, figure 3). Especially, isomers a and b are found to be degenerated in energy at PBEPA/LANL2DZ level, while isomers a and d are found to be nearly degenerated in energy at PBEPA/Au/SDD+2f/M/ECP28 MWB. Keeping in mind the inherent accuracy of the DFT, we could not exclude the probability of four isomers by DFT calculations. It is necessary to compare their simulated photoelectron spectra with the experimental photoelectron spectra. Unfortunately, without the experimental photoelectron spectra for TcAu_{16}^– cluster, we only provide theoretical photoelectron spectra in the present work. In order to compare the various local minimum structures with other 3d or 4d transition metal atom doping, we also present the first three planar shape isomers and two exohedral structures. The first three two-dimensional (2D) planar local minimum structures possess high symmetry by SK-DFT at PBEPA/Au/SDD+2f/M/ECP28MWB level. As seen from figure 2, the two 2D structures g and i have a relatively high symmetry C_{2v}, which are less stable than the ground-state structure a by 1.81 and 4.39 eV for MoAu_{16}^–. The similar situation occurred for TcAu_{16}^–, where 2D isomers g and i present the same symmetry C_{2v} and possess the higher energy than lowest-energy structure a by 1.52 and 2.43 eV. The structures with exohedral doping are all higher-lying isomers, this is in accord with the results of other 3d and 4d transition metal atoms (e.g. Sc, Ti, V, Cr, Mn, Fe, Co, Ni, Cu, Zn, Y, Zr and Nb) doping in golden cage cluster Au_{16}^– [18–20,22–24]. It is thoroughly different from the doping of a group IV atom (Si, Ge and Sn) into the Au_{16}^– cage [30], forming the exohedral gold cluster M@Au_{16}^–. Furthermore, the exohedral doping ground-state structure also occurred for C-, K- and Ag-doped golden clusters, as shown by Fa & Yang [16,32].

Table 2. Structural and energetic characteristics for the five low-lying isomers of doped cluster anions M@Au_{16}^– (M = Mo and Tc).^a

| Cluster | Structure | SM | Sym   | ΔE   | BE   | DE   | $E_{gap}$ | ADE | VDE |
|---------|-----------|----|-------|------|------|------|-----------|-----|-----|
| Mo@Au_{16}^– | a | 2 | C_{2v} | 0.00 | 2.48 | 0.29 | 0.40 | 3.24 | 3.29 |
|          | b | 2 | C_{1}  | 0.43 | 2.45 | 0.27 | 0.32 | 2.66 | 3.22 |
|          | c | 2 | C_{1}  | 0.41 | 2.45 | 0.27 | 0.32 | 3.05 | 3.16 |
|          | d | 2 | C_{1}  | 0.52 | 2.45 | 0.26 | 0.33 | 3.08 | 3.19 |
|          | e | 2 | C_{1}  | 0.66 | 2.44 | 0.25 | 0.34 | 3.00 | 3.11 |
| Tc@Au_{16}^– | a | 1 | C_{2v} | 0.10 | 2.46 | 0.28 | 0.45 | 3.10 | 3.18 |
|          | b | 5 | C_{1}  | 0.00 | 2.46 | 0.29 | 0.51 | 3.31 | 3.43 |
|          | c | 5 | C_{1}  | 0.18 | 2.45 | 0.28 | 0.24 | 2.85 | 2.96 |
|          | d | 7 | C_{1}  | 0.09 | 2.46 | 0.29 | 0.16 | 2.81 | 2.91 |
|          | f | 7 | C_{2v} | 0.22 | 2.45 | 0.28 | 0.13 | 2.94 | 3.02 |

^a Shown are the spin multiplicity (SM), symmetry type (Sym), relative energy (ΔE), binding energy (BE) per atom, doping energy (DE) per atom, HOMO–LUMO energy gap ($E_{gap}$), and calculated first ADE/VDE.
Table 2 shows the binding energy, doping energy and HOMO–LUMO gap of Mo@Au16− and Tc@Au16− clusters. For the Mo@Au16− structure, cluster a has the largest binding energy of 2.48 eV among all the isomers. The binding energy of isomers b, c, d and e is about 2.44 to 2.45 eV, which is smaller than that of the isomer a. For the doping energy, it is defined as the energy sum of the Au16− and the M atom minus the total energy of the MAu16−, as given in Table 2, the doping energy of isomer a is larger than that of other ones, indicating that isomer a has the highest stability among all the isomers. As for the HOMO–LUMO gap, it can be seen from Table 2 that isomer a has obviously higher HOMO–LUMO gap relative to isomers b, c, d and e. The HOMO–LUMO gap of isomer a is 0.40 eV, and the values of other four isomers are approximately 0.33 eV. For Tc@Au16− cluster, the binding energy and the doping energy of the lowest-energy isomers are close to each other. The values of about 2.46 and 0.28 eV are for binding energy and doping energy, respectively. For the HOMO–LUMO gap, the result of isomer b is significantly higher than those of isomers a, c, d and f, suggesting that the isomer b is the most chemically stable. The lowest-energy structures Mo@Au16−(a) and Tc@Au16−(b) stand out in the stability, as measured by their high binding energy per atom (greater than 2.46 eV), doping energy (0.29 eV) as well as a large HOMO–LUMO gap (greater than 0.40 eV).

3.2. Photoelectron spectroscopy and detachment energy

The first ADE is determined by calculating the energy difference between the optimized geometry of the anionic cluster and the optimized neutral cluster as the initial point at the anion geometry. Single-point energies of the neutral clusters are also computed based on the same optimized anion geometry. The difference in the energy of the anion and neutral cluster gives the first VDE. We examined 11 low-lying isomers by energies from the PBEPBE/Au/SDD+2f/M/ECP28MWB level, including six endohedral cages (isomers a–f), three plane structures (isomers g–i) and two exohedral doping (isomers j–k), but only one candidate (isomer a) for MoAu16− and five candidates (isomers a–d) for TcAu16− approximately 0.3 eV. In order to assist the future comparison with further experiments, we have drawn the simulated anion photoelectron spectra company with structures of the several candidate lowest-energy isomers (approximately 0.3 eV) of M@Au16− (M = Mo and Tc) in figures 4 and 5. Those isomers with the values approximately 0.3 eV from the lowest-energy isomer are all regarded as candidates for the low-lying isomers. The calculated first ADE and VDE for the top five of MAu16− (M = Mo and Tc) are presented in Table 2. The first VDE of each cluster anion corresponds to the first peak maximum of each spectrum in figures 4 and 5. The ADE/VDE of the top five of M@Au16− are 3.24/3.29 (a), 2.66/3.22 (b), 3.05/3.16 (c), 3.08/3.19 (d), 3.00/3.11 eV (e) for M = Mo, and 3.10/3.18 (a), 3.31/3.43 (b), 2.85/2.96 (c), 2.81/2.91 (d), 2.94/3.02 eV (f) for M = Tc, which are smaller than those of Au16− cage (theoretical: 3.89/4.02 eV, experimental: 3.99 ± 0.03 eV [18,27], Table 1). The energy difference between ADE and VDE is very little, e.g. the difference in energy is only 0.05 eV for Mo@Au16−(a) and 0.08, 0.12, 0.11, 0.10, 0.08 eV for Tc@Au16−(a)(b)(c)(d)(f), respectively. This is due to the negligible geometry changes between the anionic and neutral ground-state structures.

As illustrated in figures 4 and 5, the simulated spectra of the several low-lying isomers in both MoAu16− and TcAu16− are a lot different from those of the pure Au16− cage, reflecting their geometric structure with a large change, meanwhile, with a larger energy gap (X–A) than the pure cluster. Remarkably, the simulated photoelectron spectra of MAu16− (figures 4 and 5) consist of rather congested PES features with large intensity variations. However, the PES spectrum of Au16− is rather simple relative to its neighbouring sizes, does not exhibit a large energy gap like other even-sized gold clusters [66], because the tetrahedral Au16 cage is an open shell with two unpaired electrons and two extra electrons are needed to make a closed-shell 18-electron Au162− cage. The simulated PES spectrum of C2v Mo@Au16− (a) is predicted to have a low first vertical detachment energy at 3.29 eV, which is even lower than that of D2d Au16− (experimental first VDE: 4.03 ± 0.03 eV). The neutral Mo@Au16 cluster with 22 valence electrons possesses a closed-shell configuration, as evident from the theoretical PES spectrum of C2v Mo@Au16− (a) which exhibits a sizable HOMO–LUMO gap of approximately 0.40 eV, and approximately 0.14 eV larger than the experimental energy gap of Au16−. The lowest-energy structure Tc@Au16− (b) and the others isomers Tc@Au16− (a), (c), (d), (f) are separated by only 0.10, 0.18, 0.09 and 0.22 eV, respectively, at PBEPBE/Au/SDD+2f/M/ECP28MWB level. Considering the uncertainty of the DFT energies for such systems, we could not conclude which isomer structure should be assigned as the global minimum for TcAu16− cluster. Unfortunately, no gas-phase experimental photoelectron spectra literature can be acquired for TcAu16− cluster. The calculated ADE/VDE values of the top-five low-lying isomers Tc@Au16− (a)–(d) and (f) are also less than the experimental values of pure clusters Au16−. The predicted PES spectra of the top-five lowest-energy structures of Tc@Au16− are somewhat...
similar, each theoretical PES with no less than 12 relatively sharp peaks and comparatively broader HOMO–LUMO gap (X–A gap). The spectrum of lowest-energy structure Tc@Au16− (b) presents four well-resolved peaks in the binding energy range 3–4 eV followed by the less congested spectral features above 4 eV. The PES spectra of the doped cluster of Tc@Au16− with the inside Tc atom present different features from those of the parent hollow cage, suggesting that its geometric and electronic structures alter remarkably due to the addition of Tc atom. Our SK-DFT results also support this point of view, indeed, there are significant differences in their geometric structure compared with that of the pure truncated tetrahedron cage. We cannot rule out the possibility that these low-lying isomers of Tc@Au16− exist in gas-phase cluster beam by simulated PES spectra and small relative energies. However, we can predict isomer Tc@Au16− (b) to be the major species and other isomers Tc@Au16− (a), (c), (d), (f) to be the minor ones contributing to the photoelectron spectrum of TcAu16− cluster in the future experiments. It will be very interesting to measure the PES for validating our predicted results on the Mo- and Tc-doped Au16 clusters. The predicted photoelectron spectra should aid in the forthcoming experimental characterization of MAu16− (M = Mo and Tc) clusters.

4. Conclusion

We present a combined Saunders ‘Kick’ global search technique and density-functional theory study of anionic and neutral doped golden cage clusters MAu16 (M = Mo and Tc). The global minimum search revealed that the endohedral cages represent the global minimum structure for the doped gold clusters MAu16. Three different structures including endohedral cages, plane and exohedral structures are obtained using the SK-DFT method. The structures of Mo- and Tc-doped endohedral cages exhibit larger distortion from the bare gold cluster cage. Based on small relative energies, we can predict that structure Tc@Au16− (b) to be the major species and other isomers Tc@Au16− (a), (c), (d), (f) to be the minor ones contributing to the photoelectron spectrum of TcAu16− in the future experiments. Moreover, theoretical PES spectra of the leading candidate clusters also have been predicted. It will be very meaningful if the leading candidate clusters presented here could be detected by the future PES experiment for validating the existence of the Mo- and Tc-doped Au16 clusters. This structural information on low-symmetry endohedral cage clusters could be considered as the building blocks for cluster-assembled materials.

Data accessibility. The datasets supporting this article have been uploaded as part of the electronic supplementary Material.

Authors’ contributions. H.-F.L. ran the simulations and drafted the manuscript. H.-Q.W. designed the study and revised the manuscript. All authors commented on the manuscript and approved the final version.

Competing interests. We declare we have no competing interests.

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