Can Free Will Emerge from Determinism in Quantum Theory?

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“What is proved by impossibility proofs is lack of imagination” — John Bell

“Imagination is more important than knowledge” — Albert Einstein

Abstract Quantum Mechanics is generally considered to be the ultimate theory capable of explaining the emergence of randomness by virtue of the quantum measurement process. Therefore, Quantum Mechanics can be thought of as God’s wonderfully imaginative solution to the problem of providing His creatures with Free Will in an otherwise well-ordered Universe. Indeed, how could we dream of free will in the purely deterministic Universe envisioned by Laplace if everything ever to happen is predetermined by (and in principle calculable from) the actual conditions or even those existing at the time of the Big Bang?

In this essay, we share our view that Quantum Mechanics is in fact deterministic, local and realistic, in complete contradiction with most people’s perception of Bell’s theorem, thanks to our new theory of parallel lives. Accordingly, what we perceive as the so-called “collapse of the wavefunction” is but an illusion. Then we ask the fundamental question: Can a purely deterministic Quantum Theory give rise to the illusion of nondeterminism, randomness, probabilities, and ultimately can free will emerge from such a theory?

Key words: Free will, Realism, Locality, Church of the larger Hilbert space, Determinism, Parallel lives.

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1 Introduction

By the end of the 19th Century, most physicists had evolved a completely deterministic view of the world. Even though he had many precursors, such as Paul Henri Thiry, Baron d’Holbach (1770), with his very influential *Système de la Nature*, it was the great French mathematician and astronomer Pierre-Simon, marquis de Laplace (1814), who expressed in the clearest terms the philosophy according to which everything is predetermined by the initial conditions. In his *Essai philosophique sur les probabilités*, he wrote:

> We ought to regard the present state of the universe as the effect of its anterior state and as the cause of the one which is to follow. Given for one instant an intelligence which could comprehend all the forces by which nature is animated and the respective situation of the beings who compose it—an intelligence sufficiently vast to submit these data to analysis—it would embrace in the same formula the movements of the greatest bodies of the universe and those of the lightest atom; for it, nothing would be uncertain and the future, as the past, would be present to its eyes.

If Laplace were right, would there be any possibility for conscious beings to exercise free will? Anything we might imagine that we are deciding would in fact have been “written” from the initial conditions existing at the time of the Big Bang! It would seem that free will requires some form of nondeterminism or randomness; that it cannot take hold unless some events happen without a cause.\(^1\)

Even though chaos theory makes it impossible to predict the future in a fully deterministic universe as soon as there is even the tiniest imprecision on the initial conditions, these initial conditions would exist precisely according to classical physics, and thus the future would be determined, independently of our possibility of predicting it.

In the 20th Century, quantum mechanics ushered in one of the greatest revolutions in the history of science. In particular, it is generally considered to be the ultimate theory capable of explaining the emergence of randomness by virtue of a mysterious process known as the “collapse of the wavefunction”, which seems to be inherent to irreversible quantum *measurements*. Therefore, quantum mechanics can be thought of as God’s wonderfully imaginative solution to the problem of providing His creatures with free will in an otherwise well-ordered Universe. Nevertheless, Einstein so disliked the idea of true randomness in Nature that he claimed to be “convinced that *He* [God] does not throw dice” in a 1926 letter to Born (Einstein, Born and Born, 1971). Most physicists today would say that Einstein was wrong in rejecting the occurrence of truly random events. But was he?

In this essay, we share our view that quantum mechanics is in fact deterministic, local and realistic, in complete contradiction with most people’s perception of Bell’s theorem, thanks to our new theory of *parallel lives*. Accord-

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1 Nevertheless, we do acknowledge that *compatibilists* hold the belief that free will and determinism are compatible ideas, and that it is possible to believe both without being logically inconsistent. See [http://plato.stanford.edu/entries/compatibilism/](http://plato.stanford.edu/entries/compatibilism/) accessed on 29 February 2012.
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For the sake of liveliness, the nontechnical style of this essay is purposely that of a spontaneous after-dinner speech. It is meant for the enjoyment of a curiosity-driven and scientifically-minded readership who does not have prior knowledge in quantum mechanics. Occasional remarks and more rigorous details for the benefit of the expert are offered in the footnotes with no apologies for the casual reader. The next three sections review the standard notions of pure and mixed states, of entanglement, and of how one part of an entangled state can be described. Readers familiar with these notions may prefer to proceed directly with Sect. 5, which describes the Church of the Larger Hilbert Space, a central notion to this essay since it restores determinism into quantum mechanics. Section 6 attempts to go one step further in restoring also locality at the expense of realism, but it fails to do so. Then, Sect. 7 announces our new theory, which we call parallel lives, in which both locality and realism are restored in a physical world in which Bell’s inequalities are nevertheless violated. Finally, Sect. 8 discusses the implication of all of the above on the existence or not of free will, be it real or illusory.

2 Pure and mixed states

According to quantum mechanics, one has to distinguish between pure and mixed states. A pure state, generally denoted $|\Psi\rangle$ following Paul Dirac, is used to represent a state about which everything is known. For instance, $|0\rangle$ and $|1\rangle$ correspond to the classical notion of bits 0 and 1, whereas $|\Psi\rangle = \frac{1}{\sqrt{2}}|0\rangle + \frac{1}{\sqrt{2}}|1\rangle$ denotes a qubit (for “quantum bit”), whose state is an equal superposition of $|0\rangle$ and $|1\rangle$. This means that $|\Psi\rangle$ represents a state that corresponds simultaneously to classical bit values 0 and 1, each with amplitude $\frac{1}{\sqrt{2}}$. If this qubit is measured in the so-called computational basis ($|0\rangle$ vs. $|1\rangle$), standard quantum mechanics has it that it will collapse to either classical state $|0\rangle$ or $|1\rangle$, each with a probability given by the square of the norm of the corresponding amplitude, here $|\frac{1}{\sqrt{2}}|^2 = \frac{1}{2}$ for each alternative. Even though the specific result of the measurement is not determined by the pure state, and two strictly identical particles in that same state could yield different results following the same measurement, the probabilities associated with such measurement outcomes are known exactly. Furthermore, this particular state would behave in a totally deterministic manner if subjected to a different measurement, known in this case as the Hadamard measurement (or measurement in the Hadamard basis “$H$”), which asks it to “choose” between $H|0\rangle = \frac{1}{\sqrt{2}}|0\rangle + \frac{1}{\sqrt{2}}|1\rangle$ and $H|1\rangle = \frac{1}{\sqrt{2}}|0\rangle - \frac{1}{\sqrt{2}}|1\rangle$. In this case, our state would choose the former since in fact $|\Psi\rangle = H|0\rangle$. Peres (1995) defined a pure state
as one for which there exists a complete measurement (which he calls a “maximal test”) under which it behaves deterministically.

In contrast, mixed states are used when there is intrinsic uncertainty not just about the result of some measurement but about the result of all possible complete measurements, hence about the state itself. One way to picture a mixed state is to think of a black box inhabited by a Daemon. When a user pushes a button, the Daemon spits out a state that it chooses at random, say with equal probability between $$|0\rangle$$ and $$|1\rangle$$. Such a mixed state would be denoted

$$\mathcal{E}_1 = \{(|0\rangle, 1/2), (|1\rangle, 1/2)\}. \quad (1)$$

More generally, a mixture of $$k$$ different pure states is denoted

$$\mathcal{E} = \{(|\Psi_1\rangle, p_1), (|\Psi_2\rangle, p_2), \ldots, (|\Psi_k\rangle, p_k)\} = \{(|\Psi_i\rangle, p_i)\}_{i=1}^k, \quad (2)$$

which means that the Daemon chooses some $$|\Psi_i\rangle$$ with probability $$p_i$$, $$1 \leq i \leq k$$, where the probabilities sum up to 1. It is legitimate to wonder if such a state is pure since the Daemon knows which $$|\Psi_i\rangle$$ it chose, or if it is mixed since the user does not know. In a sense it is both. Nevertheless, no measurement chosen by the user will provide a deterministic answer. For instance, a measurement of $$\mathcal{E}_1$$ in the computational basis will reveal the Daemon’s random choice, which has equal probability $$1/2$$ of being $$|0\rangle$$ or $$|1\rangle$$. On the other hand, a measurement in the Hadamard basis will produce $$H|0\rangle$$ or $$H|1\rangle$$ with equal probability $$1/2$$ since such would be the case regardless of whether the Daemon had spit out $$|0\rangle$$ or $$|1\rangle$$. Thus we see that the randomness lies with the Daemon in one case and with the user’s measurement in the other case, but the final result is the same. More interestingly, it can be demonstrated that any measurement on $$\mathcal{E}_1$$ that would ask it to choose between two arbitrary one-qubit orthogonal states would choose either one with equal probability. (Two states are orthogonal if it is possible in principle to distinguish perfectly between them, such as $$|0\rangle$$ and $$|1\rangle$$, or $$H|0\rangle$$ and $$H|1\rangle$$.)

By Peres’ definition, $$\mathcal{E}_1$$ is not pure since there does not exist a complete measurement under which it behaves deterministically.

Mixed states can be described as above by a mixture of pure states, but they can also be described in two other ways. One of them is known as the density matrix (aka density operator). This is a matrix (an array of numbers) that can be calculated mathematically from the more intuitive mixture $$\{(|\Psi_i\rangle, p_i)\}_{i=1}^k$$ of pure states. The remarkable fact about density matrices is that different mixtures can give rise to the same matrix, yet this matrix represents all that is measurable about the state, by any measurement whatsoever “allowed” by quantum mechanics. For instance, the density matrix that is computed from Eq. (1) is identical to that arising from the apparently different mixture

\[\text{This must be a true random choice, possibly implemented by a quantum-mechanical process; flipping a classical coin would not suffice here.} \]
In other words, if we trust a Daemon to send us an equal mixture of $|0\rangle$ and $|1\rangle$ (Eq. 1) but in fact it provides us with an equal mixture of $H|0\rangle$ and $H|1\rangle$ (Eq. 3), we shall never be able to notice that it is “cheating”!

Given that these two mixtures are impossible to distinguish, it makes sense to consider the corresponding mixed states as actually identical. Just for completeness, notice that even mixtures featuring more than 2 pure states can be indistinguishable from those above. For instance, mixture

$$E_3 = \{(|0\rangle, \frac{1}{3}), (\frac{1}{2}|0\rangle + \frac{\sqrt{3}}{2}|1\rangle, \frac{1}{3}), (\frac{1}{2}|0\rangle - \frac{\sqrt{3}}{2}|1\rangle, \frac{1}{3})\} \quad (4)$$

is indistinguishable from (hence identical to) mixtures $E_1$ and $E_2$ because it gives rise to the same density matrix.

We postpone until Sect. 5 discussion of the third way—by far the most interesting—in which one may think of mixed states.

### 3 Entanglement

The concept of entanglement was first published (although not named) by [Einstein, Podolsky and Rosen (1935)](https://en.wikipedia.org/wiki/Einstein%E2%80%93Podolsky%E2%80%93Rosen_paradox) in a failed attempt to demonstrate the incompleteness of the quantum formalism. However, there is historical evidence that the notion had been anticipated by Schrödinger several years previously, who was quick to understand the importance of entanglement:

“I would not call that one but rather the characteristic trait of quantum mechanics, the one that enforces its entire departure from classical lines of thought” [Schrödinger (1935)](https://en.wikipedia.org/wiki/Erwin_Schr%C3%B6dinger). We could not agree more with this assessment. Our quantum world is not classical because, as spectacularly demonstrated by [Bell (1964)](https://en.wikipedia.org/wiki/John_Bell), entanglement cannot be explained by any classical local realistic theory of the sort that was so dear to Einstein. (Or can it? We’ll come back to this question in Sect. 7.) Indeed, we consider entanglement to be the key to understanding Nature. We would even go so far as to say that it’s our best window into probing the soul of the Universe. The other non-classical aspects of quantum mechanics, such as the quantization of energy and its consequence on the photoelectric effect—which earned Einstein his Nobel Prize in 1921—are no doubt important, but lag far behind the magic of entanglement on our personal wonder scale.

Entanglement is a phenomenon by which two (or more) physically separated systems must sometimes be thought of as a single (nonlocal) entity.

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3 A much more remarkable example of cheating is possible for a Daemon who would be “paid” to produce randomly chosen Bell states. It could produce instead pairs of purely classical uncorrelated random bits. These mixtures being identical in terms of density matrices, such cheating would be strictly undetectable by the user. This is profitable for the Daemon because classical bits are so much easier to produce than Bell states!
The simplest example of entanglement is known as the singlet state,

\[ |\Psi^-\rangle = \frac{1}{\sqrt{2}} |01\rangle - \frac{1}{\sqrt{2}} |10\rangle, \]

which consists of two particles. A measurement of both particles in the computational basis results in either outcome \( |01\rangle \) or \( |10\rangle \), each with equal probability since \( |\pm 1/\sqrt{2}|^2 = 1/2 \). Here, outcome \( |01\rangle \) means that the first particle is measured as \( |0\rangle \) and the second as \( |1\rangle \), and similarly for outcome \( |10\rangle \). In other words, the two particles yield opposite answers when they are measured in the computational basis. So far, this is not more mysterious than if someone had flipped a penny, sliced it through its edge, put each half-penny in an envelope, and mailed the envelopes to two distant locations. When the envelopes are opened (“measured”), there is no surprise in the fact that each one reveals a seemingly random result (heads or tails) but that the two results are complementary. Such an explanation would correspond to purely classical mixed state

\[ \mathcal{E}_0 = \{ (|01\rangle, 1/2), (|10\rangle, 1/2) \}, \]

where \( |0\rangle \) stands for heads and \( |1\rangle \) stands for tails.

What makes this singlet state so marvellous is that quantum mechanics asserts that \( |\Psi^-\rangle \) is indeed the pure state given in Eq. (5) and not the mixed state of Eq. (6), and that those are very different indeed. In particular, the result of any measurement is not predetermined (as it would be with the half-penny analogy): it comes into existence only as a result of the measurement itself. This is particularly mysterious when the two particles are arbitrarily far apart because it is as if they were magic coins which, when flipped, always provide opposite, yet freshly random, outcomes. In fact, the two particles provide opposite answers to any complete measurement, provided they are subjected to the same one. It’s like an old couple who disagrees on any question you may ask them... even when they don’t have a clue about the answer and hence respond randomly! This phenomenon can be “explained” by elementary linear algebra, according to which state \( |\Psi^-\rangle \), as given in Eq. (5), is mathematically equivalent to

\[ |\Psi^-\rangle = \frac{1}{\sqrt{2}} |\psi\rangle|\phi\rangle - \frac{1}{\sqrt{2}} |\phi\rangle|\psi\rangle \]

for any two one-qubit orthogonal states \( |\psi\rangle \) and \( |\phi\rangle \), such as H\( |0\rangle \) and H\( |1\rangle \). It is important to understand that this behaviour would not occur with the mixed state of Eq. (6) because, in that case, asking the two particles to “choose” between H\( |0\rangle \) and H\( |1\rangle \) would produce two random and uncorrelated outcomes.

An entangled state such as the singlet behaves exactly as if the first particle, when asked by a measurement to choose between orthogonal states \( |\psi\rangle \) and \( |\phi\rangle \), flipped a fair coin to decide which one to select, and then “instructed” the other particle to instantaneously assume the opposite state. This gives the impression of instantaneous action at a distance, a concept that so revolted
Einstein that he derisively called it *spukhafte Fernwirkungen* (“Spooky action at a distance”). But is this really what happens or is it only a naïve “explanation”? We shall come back to this most fundamental issue in Sects. 6 and 7.

It has been experimentally demonstrated that if indeed the particles had to communicate, then the effect of the first measurement on the second particle would have to take place at least ten thousand times faster than at the speed of light (Salart, Baas, Branciard, Gisin and Zbinden, 2008). Even more amazingly, relativistic experiments have been performed, following a fascinating theoretical proposal by Suarez and Scarani (1997), in which the predictions of quantum mechanics continue to hold even when the two particles move apart quickly enough that they are both measured before the other in their respective inertial reference frames (Stefanov, Zbinden, Gisin and Suarez, 2002). These remarkable experiments make it untenable to claim that the first measured particle somehow sends a signal to tell the other how to behave. This has prompted Gisin (2012) to assert that quantum correlation “emerge from outside space-time”.

We highly recommend the exceptionally lucid and entertaining popular accounts of some classically-impossible marvels made possible by entanglement that have been written by Mermin (1981, 1994) for the American Journal of Physics.

4 Describing one part of an entangled state

The defining characteristic of a pure entangled state split between two distant locations is that neither of the local subsystems can be described as a pure state of its own. This should be clear from Peres’ definition of a pure state and the fact that each part of an entangled state is so that its outcome is not predetermined, no matter to which complete measurement it is subjected. Nevertheless, it makes sense to wonder if there is a way to describe the state of one of the subsystems.

One natural approach is to see what would happen if we measured the other subsystem. Consider for instance the singlet state $|\Psi^-\rangle$ and let us measure one of the particles in the computational basis. We have seen that the outcome is $|0\rangle$ (resp. $|1\rangle$) with probability $1/2$, in which case the other system is now in state $|1\rangle$ (resp. $|0\rangle$). Therefore, if one system is measured and one forgets the outcome of the measurement, the unmeasured system is in state $|0\rangle$ with probability $1/2$ and in state $|1\rangle$ also with probability $1/2$. In other words, this system is in mixed state $\mathcal{E}_1$, according to Eq. (1). But the first system could have been measured in the Hadamard basis instead. Depending on the result of this measurement, the unmeasured system would then be left either in state $\mathcal{H}|0\rangle$ or $\mathcal{H}|1\rangle$, each with probability $1/2$. If we forget again the result of the measurement, the unmeasured system is therefore in mixed state $\mathcal{E}_2$, according to Eq. (3). Now, remember that mixtures $\mathcal{E}_1$ and $\mathcal{E}_2$ are considered...
to be identical since they give rise to the same density matrix. More generally, it can be demonstrated from the formalism of quantum mechanics that no matter which complete measurement is performed on one subsystem of an arbitrary entangled state, the other subsystem always ends up in the same mixed state in terms of a density matrix, albeit not necessarily according to the same mixture of pure states.

It follows that nothing can be more natural than to describe one subsystem of an entangled state by the mixed state in which this subsystem would be left if the other subsystem were measured. This is well-defined since the resulting density matrix does not depend on how the other subsystem is measured. If we carry this reasoning to its inescapable conclusion, it makes sense to describe the state of a subsystem in this way even if the other subsystem has not been measured yet, indeed even if it is never to be measured. When we consider the state of a subsystem of an entangled state in this way, we say that we trace out the other subsystem.

Section 3 may have left you with the impression that entanglement requires instantaneous communication, which would be incompatible with Einstein’s special theory of relativity. If we remember that the density matrix describes all that can be measured about a quantum system, however, it follows from the above discussion that entanglement cannot be used to signal information between two points in space since no operation performed on one subsystem of an entangled state can have a measurable effect on the other subsystem. It is as if quantum systems were capable of instantaneous communication, but only in tantalizing ways that could not be harnessed by us, macroscopic humans, to establish such communication between ourselves. We shall come back on the consequences of this crucial issue in Sects. 6 and 7.

5 Church of the Larger Hilbert Space

We have just seen that the state of any subsystem of a pure (or, for that matter, mixed as well) entangled state can be expressed as a mixed state in a unique and natural way. It is remarkable that the converse holds. We saw in Sect. 2 that mixed states can be described either as mixtures of pure states (possibly under the control of a Daemon) or as density matrices, but we promised a third way and here it is. Any mixed state can be described as the trace-out of some subsystem from an appropriate pure state. Such a pure state is called a purification of the mixed state under consideration.

There is an easy way (theoretically speaking) to construct a purification of an arbitrary mixture $\mathcal{E} = \{(\Psi_i, p_i)\}_{i=1}^k$. For this, consider some other quantum system that could be in any of $k$ orthogonal states $|\Phi_1\rangle$, $|\Phi_2\rangle$, $\ldots$, $|\Phi_k\rangle$ and consider pure state
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\[ |\Psi\rangle = \sum_{i=1}^{k} \sqrt{p_i} |\Psi_i\rangle |\Phi_i\rangle , \]

where \(\sum_{i=1}^{k} \) serves to denote a quantum superposition on \( k \) pure states. If the right-hand subsystem of \( |\Psi\rangle \) were measured by asking it to "choose" between one of the \( |\Phi_i\rangle \)'s, each \( |\Phi_i\rangle \) would be chosen with probability \( |\sqrt{p_i}|^2 = p_i \), leaving the unmeasured left-hand subsystem in state \( |\Psi_i\rangle \).

Now, imagine that it were our friend the Daemon who prepared pure state \( |\Psi\rangle \) and measured its right-hand subsystem. By learning which \( |\Phi_i\rangle \) is obtained, with probability \( p_i \), the Daemon would know in which pure state \( |\Psi_i\rangle \) the unmeasured subsystem is. If the Daemon spits out this subsystem to the user, without revealing the result of the measurement, the user receives a mixed state corresponding to mixture \( E \). As in Sect. 2, this system is in a pure state for the Daemon and in a mixed state for the user. The beauty of this concept is that it works even if the Daemon has not, in fact, measured the right-hand subsystem of the pure state it had created. Even better, it still works if the Daemon has destroyed that right-hand subsystem, inasmuch as a quantum state can be destroyed, to prevent any temptation to measure it later and sell the answer to the user! In this case, the surviving quantum system would be in mixed state \( E \) not only for the user, but also for the Daemon.

The fact that any mixed state can be considered as the trace-out of one of its purifications is the fundamental tenet of the Church of the Larger Hilbert Space, a term coined by John Smolin because the formalism of quantum mechanics has pure quantum states inhabit so-called Hilbert spaces and any mixed state can be thought of as a subsystem from a pure state than lives in a larger Hilbert space.

Everything that we have explained so far in this essay corresponds to strictly orthodox quantum mechanics and no (serious) physicist would disagree with a single word from it. From this point on, however, we articulate our personal beliefs concerning the world in which we live, which are admittedly very similar to the "relative state" formulation of quantum mechanics put forward by Everett (1957) more than fifty years ago; see also Byrne (2007).

The weak Faithfuls in the Church of the Larger Hilbert Space believe in the fact that any mixed state can be thought of as the trace-out of some imaginary purification, but this is only for mathematical convenience. In fact, it is not possible to believe in the predictions and formalism of quantum mechanics without being (at least) a weak faithful since the (mathematical) existence of a purification for any mixed state is a theorem that can be derived from first principles.

The strong Faithfuls—among whom we stand—believe that to any mixed state that actually exists, there corresponds somewhere in the Universe an appropriate purification. This is an extremely far-reaching belief since it implies (among other things) that the "collapse of the wavefunction", which
orthodox quantum mechanics associates with measurements, is but an illusion. In fact, strong belief in the Church implies that quantum mechanics is strictly unitary and therefore reversible. If we forget for simplicity the necessity to apply relativistic corrections, the Universe is ruled by one law only, known as Schrödinger’s equation. This equation is deterministic—even linear—and therefore so is the entire evolution of the Universe.

Let us consider for instance the simplest case of orthodox collapse of the wavefunction: the measurement of a single diagonally-polarized photon (a particle of light) by an apparatus that distinguishes between horizontal and vertical polarizations. For definiteness, consider a calcite crystal that splits an incoming light beam between horizontally and vertically polarized sub-beams followed by two single-photon detectors (which we assume perfect for sake of the argument). Any horizontally-polarized photon would cause one of the two detectors to react, whereas a vertically-polarized photon would cause the other detector to react. According to orthodox quantum mechanics, a diagonally-polarized photon would hit the crystal and then continue in quantum superposition of both paths until it hits both detectors. At this point, one (and only one) of the detectors would “see” the photon and produce a macroscopic effect that would be detectable by the (human) observer. For some, the phenomenon would become irreversible as soon as it has had a macroscopic effect inside the detector; for others only when some observer becomes conscious of the outcome.

According to the Strong Church of the Larger Hilbert Space, neither is the case: the diagonally-polarized photon is in fact in an equal superposition of being horizontally and vertically polarized (so far, this is in strict accordance with orthodox quantum mechanics) and the crystal merely puts the photon in a superposition of both the horizontally and vertically polarized paths (still in accordance with orthodox quantum mechanics). But when the photon hits both detectors, it becomes entangled with them. The composite system photon-detectors is now in an equal superposition of the photon being horizontally-polarized and the horizontal-polarization detector having reacted with the photon being vertically-polarized and the vertical-polarization detector having reacted. And when the observer looks at the detectors, he or she becomes entangled with the photon-detector system so that now the photon-detector-observer system is in an equal superposition of the photon being horizontally-polarized, the horizontal-polarization detector having reacted and the observer having seen the horizontal-polarization detector reacting with the same events corresponding to a vertically-polarized photon.

From this perspective, there is no collapse. The horizontal detection is as real as the vertical one. But any (human) observer becomes aware of only one outcome, and here lies the apparent paradox. If indeed both events occur (in quantum superposition), how come our experience makes us (humans) believe that only one outcome (apparently chosen at random by Nature) has
actually occurred? In his groundbreaking paper, Everett (1957) proposed the following analogy:

Arguments that the world picture presented by this theory is contradicted by experience, because we are unaware of any branching process, are like the criticism of the Copernican theory that the mobility of the earth as a real physical fact is incompatible with the common sense interpretation of nature because we feel no such motion. In both cases the argument fails when it is shown that the theory itself predicts that our experience will be what it in fact is. (In the Copernican case the addition of Newtonian physics was required to be able to show that the earth’s inhabitants would be unaware of any motion of the earth.)

In other words, it is not because we (humans) cannot feel the Earth moving under our feet that it stands still at the centre of the Universe! Similarly, it is not because we cannot feel the Universal superposition that it does not exist. According to the Strong Church of the Larger Hilbert Space, the Earth as we feel it has but a tiny amplitude in the Universal wavefunction, and each one of us has an even tinier amplitude. This perspective is very humbling indeed, much more so than accepting the insignificance of the Earth within the classical Universe, but this is nevertheless the perspective in which we most passionately believe.

It remains to see how the Church of the Larger Hilbert Space can account for the phenomenon described in Sect. 3 when we discussed the measurement of far-apart entangled particles. Consider again two particles in the singlet state (Eq. 5) and assume that they are both subjected to the same measurement, which asks them to “choose” between orthogonal states $|\psi\rangle$ and $|\phi\rangle$.

We can think of the two particles as being in the state given by Eq. (7), which once again is mathematically equivalent to Eq. (5), and initially the measurement apparatuses have not reacted, so that they are not entangled with the particles. The joint state of the apparatus-particle-particle-apparatus system can therefore be described as

$$\left|\frac{1}{\sqrt{2}}\psi\rangle \phi\rangle + \frac{1}{\sqrt{2}}\phi\rangle \psi\rangle \right| \left|\frac{1}{\sqrt{2}}\psi\rangle \phi\rangle - \frac{1}{\sqrt{2}}\phi\rangle \psi\rangle \right|,$$

where $|?\rangle$ represents a measurement apparatus that has not yet reacted. This is mathematically equivalent to

$$\frac{1}{\sqrt{2}}|??\rangle|\psi\rangle|\phi\rangle - \frac{1}{\sqrt{2}}|??\rangle|\phi\rangle|\psi\rangle.$$  

Let us say without loss of generality that the particle on the left is measured first. According to the Church of the Larger Hilbert Space, this has the effect of entangling it with its measurement apparatus. However (and

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4 Of course, we must account for all the nonclassical correlations that violate various forms of Bell inequalities, not only for the (classically explicable) fact that two particles in the singlet state will always give opposite answers when subjected to the same measurement. This paragraph can be adapted mutatis mutandis to any pair of measurements, including POVMs, on an arbitrary bipartite entangled state, as well as to similar scenarios for multipartite entanglement.
contrary to the teachings of standard quantum mechanics), the two particles remain entangled, albeit no longer in the singlet state. Now, the joint state of the complete system has (unitarily) evolved to
\[
\left( \frac{1}{\sqrt{2}} |\Psi\rangle |\psi\rangle + \frac{1}{\sqrt{2}} |\Phi\rangle |\phi\rangle \right) |?\rangle,
\]
where $|\Psi\rangle$ (resp. $|\Phi\rangle$) represents the state of a measurement apparatus that has registered a particle in state $|\psi\rangle$ (resp. $|\phi\rangle$). Note that the apparatus on the right is still unentangled with the other systems under consideration. Finally, when the particle on the right is measured, the system evolves to
\[
\frac{1}{\sqrt{2}} |\Psi\rangle |\psi\rangle |\phi\rangle + \frac{1}{\sqrt{2}} |\Phi\rangle |\phi\rangle |\psi\rangle |\Psi\rangle.
\]
(11)
At this point, if we trace out the two particles, the detectors are left in mixed state
\[
\left\{ (|\Psi\rangle |\Phi\rangle, 1/2), (|\Phi\rangle |\Psi\rangle, 1/2) \right\},
\]
(12)
which is exactly as it should: they have produced random but complementary outcomes. Naturally, we could also involve two human observers in this scenario. If we had, they would enter the macroscopic entangled state of Eq. (11): at that point, they would be in a superposition of having seen the two possible complementary sets of outcomes, but they would be blissfully unaware of this.

As an amusing anecdote, we cannot resist mentioning the (real-life!) venture called cheap universes.\(^5\) For a mere $3.95, or unlimited use for $1.99 on an iPhone, you can select two courses of action (such as “I shall either go on a hike, or I shall take a nice hot bath”) and ask cheap universes to make a purely quantum choice between the two alternatives.\(^6\) Provided you have self-pledged to obey the outcome, you may proceed lightheartedly because you know that you are also performing the other action in the Universal wavefunction. Indeed, should the consequences of having indulged in a nice hot bath turn out to be disastrous, you can take comfort in knowing that you have also gone on a hike and hope that this was indeed the path to happiness. Sounds crazy? Not to us!

The Strong Church of the Larger Hilbert Space is different from (but not incompatible with) the so-called Many-World Interpretation of Quantum Mechanics (usually associated with the name of Everett) in the sense that we believe in a single Universe—not in the “Multiverse” advocated by the Many-World Interpretation followers—but one in which quantum mechanics

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\(^5\) [http://www.cheapuniverses.com](http://www.cheapuniverses.com) accessed on 29 February 2012.

\(^6\) Specifically, cheap universes uses a commercial device called QUANTIS, available from ID Quantique, in which “photons are sent one by one onto a semi-transparent mirror and detected; the exclusive events (reflection/transmission) are associated to ‘0’/‘1’ bit values”. See [http://www.idquantique.com/true-random-number-generator/products-overview.html](http://www.idquantique.com/true-random-number-generator/products-overview.html) accessed on 29 February 2012. According to our example, we would associate outcome 0 with “I shall go on a hike” and outcome 1 with “I shall take a nice hot bath”.
rules at face value: We (poor humans) perceive only what we call the classical states, but arbitrarily complex superpositions of them do in fact exist in reality.

6 Can locality be restored outside of the Church?

Einstein thought that quantum mechanics must be incomplete because it did not fulfill his wish for a local and realistic theory. We distinguish between strong realism, according to which any property of a physical system registered by a measurement apparatus (or by any other process by which the system is observed) existed prior to the measurement, so that the apparatus merely reveals what was already there, and weak realism, according to which a physical system can respond probabilistically to a measurement apparatus, but the probability distribution of the possible outcomes exists prior to the measurement. For instance, the diagonal polarization of a horizontally-polarized photon exhibits weak realism according to quantum mechanics because its measurement behaves randomly, yet with well-defined probabilities (in this case with equal probability of registering a $+45^\circ$ or a $-45^\circ$ outcome).

Similarly, we distinguish between strong locality, according to which no action performed at point A can have an effect on point B faster than the time it takes light to go from A to B, and weak locality, according to which there can be no observable such effect. As we have seen already, if two particles are jointly in the singlet state (Eq. 5) and if one is measured, yielding outcome $|0\rangle$, the other particle behaves as if its state had instantaneously changed from being half a singlet to pure state $|1\rangle$, no matter how far apart the two particles are. Even though this phenomenon seems to violate strong locality (we shall come back on this issue below and in the next section), it is important to understand that it does not violate weak locality because the instantaneous effect (if it exists) cannot be detected by any process allowed by quantum mechanics. Taking account of the special theory of relativity, violations of weak locality would enable reversals in causality (effects could precede causes), whereas violations of strong locality have no such spectacular consequences. Fortunately, quantum mechanics does not allow any violation of weak locality. From now on, “locality” will be understood to mean “strong locality” unless specified otherwise.

For a strong faithful in the Church of the Larger Hilbert Space, the issue of locality can take different flavors. At one extreme, the wavefunction is the one and only reality and the question does not even make sense. The universe is in a massive superposition and anything that appears to involve a random quantum choice in one branch of the superposition “simply” makes the universal superposition more complicated; the issue of locality does not even spring up. This position is often considered to be a “cop out” by those
who are not faithfuls of the Church, who think that believers are simply avoiding the issue rather than trying to explain it. The other extreme among the faithfuls is populated by the advocates of the many-world interpretation of quantum mechanics, some of whom consider that the entire world splits up each time a random quantum choice appears to be made. Such a split is highly nonlocal if it is instantaneous. In the next section, we shall present our \textit{parallel lives} interpretation of the Church of the Larger Hilbert Space, which is fully compatible with locality. In the rest of this section, however, we shall step outside of the Church and attempt to reconcile locality with quantum mechanics while denying the possibility for macroscopic objects (such as human observers) to enter into a superposition.

The great discovery of Bell (1964), or so it seems, is that the predictions of quantum mechanics are incompatible with any possible strongly local and weakly realistic theory of the world.\footnote{To be historically more accurate, Bell’s original 1964 paper was concerned with strong realism only, but it can be strengthened to take account of weak realism.} Since quantum mechanics has been vindicated by increasingly sophisticated experiments (Freedman and Clauser, 1972; Aspect, Grangier and Roger, 1981; Aspect, Dalibart and Roger, 1982; Aspect, Grangier and Roger, 1982; Stefanov, Zbinden, Gisin and Suarez, 2002; Salart, Baas, Branciard, Gisin and Zbinden, 2008, etc.), most physicists infer that there is no other choice but to forego locality. However, we beg to disagree on the inevitability of this conclusion. If the world cannot be simultaneously local and realistic, could locality be restored at the expense of realism?

One may attempt to achieve this by accepting that the state of a quantum system is fundamentally \textit{subjective} (or to be technically more exact, \textit{epistemic}). For instance, the same particle can be in one state for one observer and in a different state for another. \textit{And both observers can be perfectly correct about the state of the particle!} However, they must have \textit{compatible} beliefs in the sense that there must exist at least one pure state that is excluded by neither observer.\footnote{To be technically exact and much more general, there must exist at least one \textit{ontic} state compatible with both \textit{epistemic} beliefs, unless we are ready to accept that there is no underlying reality at all (Pusey, Barrett and Rudolph, 2011).}

For sake of the argument, consider again a quantum system in the singlet state (Eq. \ref{eq:singlet}) so that the two particles are arbitrarily far apart, say at points A and B, which are inhabited by Alice and Bob, respectively. We have seen that the state of either particle can be described locally by mixture $\mathcal{E}_1$ from Eq. (\ref{eq:local}). To stress that we are not talking about the \textit{specific} mixture of pure states explicit in $\mathcal{E}_1$ (since the state of these particles can just as well be described by mixtures $\mathcal{E}_2$ or $\mathcal{E}_3$), let us denote the corresponding density matrix by $\rho$, which is uniquely defined.

Consider what happens if Alice measures her particle in the computational basis and obtains (say) outcome $\vert 0 \rangle$. Then, assuming Bob has not interacted with his particle, Alice knows that Bob’s particle is no longer in mixed state $\rho$:
now it is in state $|1\rangle$. But for Bob, nothing has changed! His particle was in state $\rho$ before Alice’s measurement and it still is in this same state immediately after the far-away measurement. In other words, the particle at point $B$ is in state $|1\rangle$ for Alice and in state $\rho$ for Bob, and both observers are correct in their assertions concerning the same particle. This is reminiscent of the proverbial Indian story of the blind men and an elephant.

The effect of Alice’s measurement can propagate to Bob, but only if a classical message transits between them. However, such a message cannot travel faster than at the speed of light. It follows that there is no faster-than-light change in the state of the particle at point $B$, as seen by Bob from that point. More generally, no operation performed at any point in space can have an instantaneous observable effect on any other point. Seen this way, no cause can have an effect faster than at the speed of light, causality is not violated, and Einstein can rest in peace.

Naturally, it is possible for an observer to be wrong about the state of a particle. For instance, if Alice prepares a particle in state $|0\rangle$ and sends it to Bob, who is far away, and if Bob subjects it to a Hadamard transformation without telling Alice, then Alice may think that the particle is still in state $|0\rangle$ and be wrong since it is now in state $\mathcal{H}|0\rangle$. However, this is not in contradiction with the above: It is not because the same particle can be in two different states according to two different observers and that both can be correct that anybody who has some opinion about the state of a quantum system is necessarily right! For Alice to know the state of a far-away particle, even subjectively, she must know what has happened to it after it left her hands. We shall therefore consider for simplicity a bipartite scenario in which each party knows what the other party is doing.

Can we completely restore locality at the expense of realism with this line of approach? Unfortunately, there is a serious problem. Consider again the case of Alice and Bob sharing a singlet state and of Alice measuring her particle. We argued above that Alice and Bob can both be correct if Alice thinks of Bob’s particle as being in state $|1\rangle$ whereas Bob thinks of it as being in mixed state $\rho$. But now, if Bob decides to measure his particle, and if indeed his belief that it is in state $\rho$ were correct, there would be no local reason that would prevent him from registering outcome $|0\rangle$, which is indeed possible when measuring $\rho$ since it can be thought of as mixed state $\mathcal{E}_1$ from Eq. 1. This would no longer be compatible with Alice’s belief that Bob’s particle is in state $|1\rangle$, even though each party knows what the other is doing. Furthermore, if they meet in the future and compare notes, Alice and Bob will register correlations that are not in accordance with quantum mechanics. (Please remember that this section is written under the assumption that neither Alice nor Bob can be in a superposition of having seen both results.)

Does it follow that quantum mechanics cannot be explained by a local theory even if we are willing to forego realism? It turns out that we can...
have our cake and eat it too, provided we reintegrate the Church of the Larger Hilbert Space. Contrary to the prevalent belief, the laws of nature can be simultaneously local and realistic, and yet obey all the predictions of quantum mechanics. In order to reconcile this claim with Bell’s impossibility proof, please consider the quotation of Bell’s at the opening of this essay and read on.

7 Parallel Lives

We shall fully develop our parallel lives theory for quantum mechanics in a subsequent paper. Here, for simplicity, we explain how local realism can be consistent with bipartite correlations that are usually considered to be even more nonlocal than those allowed by quantum mechanics. Specifically, we consider the so-called nonlocal box introduced by Popescu and Rohrlich (1994), which we illustrate with a tale that takes place in an imaginary world, i.e. in a toy model of an alternative universe. Our universe follows Einstein’s special theory of relativity so that it is possible to assert, according to the principle of weak locality, that some events cannot influence the outcome of other far-away events that are sufficiently simultaneous.

Imagine two inhabitants of this universe, Alice and Bob, who travel very far apart in their spaceships. Each one of them is carrying a box that features two buttons, labelled 0 and 1, and two lights, one green and one red. Once they are sufficiently distant, Alice and Bob independently flip fair coins to decide which button to push on their boxes, which causes one light to flash on each box. The experiment is performed with sufficient simultaneity that Alice’s box cannot know the result of Bob’s coin flip (hence the input to Bob’s box) before it has to flash its own light, even if a signal travelling at the speed of light left Bob’s spaceship at the flip of his coin toss to inform Alice’s box of the outcome, and vice versa.[10]

After several instances of this experiment, Alice and Bob meet again to compare their results. They discover to their amazement that they saw different colours when and only when they had both pushed the “1” button. In a local classical world that denies the Church of the Larger Hilbert Space, in which Alice and Bob cannot enter into a superposition (as in the previous section), it is easy to see that such boxes cannot exist. More precisely, the best box that can be built cannot produce such results with a probability better 75%. In a quantum-mechanical world, we can do better by the magic

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[10] We are implicitly ruling out the local realistic theory of superdeterminism here, according to which there is no way to prevent the boxes from knowing which button is pressed on the other box, not because a signal travels quickly enough between the boxes, but because everything being deterministic, each box knows everything about the future, including which buttons will be pushed anywhere in the universe. See [http://en.wikipedia.org/wiki/Superdeterminism](http://en.wikipedia.org/wiki/Superdeterminism) accessed on 29 February 2012.
of entanglement, but the success probability cannot exceed \(\cos^2 \pi/8 \approx 85\%\) \cite{Cirel'son1980}, hence our imaginary world is not ruled by quantum mechanics either. This is fine: remember that the purpose of this scenario is not to suggest a model of our world, but rather to show that it is possible in a local realistic world to violate a Bell inequality.

What is the trick? Imagine that each spaceship lives inside a bubble. When Alice pushes one button on her box, her bubble splits into two parallel bubbles. Each bubble contains a copy of the spaceship and its inhabitant. Inside one bubble, Alice has seen the red light flash on her box; inside the other bubble, she has seen the green light flash. From now on, the two bubbles are living parallel lives. They cannot interact between themselves in any way and will never meet again. The same phenomenon takes place when Bob pushes one button on his box. Please note that Alice’s action has strictly no instantaneous influence on Bob’s bubble (or bubbles if he has already manipulated his box): this splitting into parallel lives is a strictly local phenomenon.

Let us consider what happens if Alice and Bob, each of whom now lives inside two parallel bubbles although they cannot feel it in any way decide to travel towards each other and meet again. (A similar scenario can be involved if they decide to use classical communication in order to compare notes, rather than travelling.) This is where magic takes place: Each of the two bubbles that contains Alice is allowed to interact and see only a single bubble that contains Bob, namely the bubble that satisfies the conditions described above. Note that such a perfect matching is always possible. Furthermore, each bubble can “know” with which other bubble to interact provided it keeps a (local) memory of which button was pressed and which light flashed. In this way, each copy of Alice and Bob will be under the illusion of correlations that “emerge from outside space-time” \cite{Gisin2012}. Yet these correlations take place fully within space and time, in a completely local realistic universe.

Let us stress again that we are not claiming that our universe actually works as described above, because it does not, according to Cirel’son \cite{Cirel'son1980}. Our point is that it is generally recognized that nonlocal boxes of the sort we have described cannot exist in any local realistic world, and this is false according to our toy model. To be more dramatic, consider Bell’s theorem, or more precisely its best-known incarnation, the CHSH inequality due to \cite{Clauser1969}. This inequality states that “in any classical theory […] a particular combination of correlations lies between \(-2\) and \(2\)” \cite{Popescu1994}. The original purpose of this inequality is that it is violated by quantum mechanics since the same “particular combination of correlations” is predicted to be equal to \(2\sqrt{2}\).

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11 Remember Everett’s analogy with medieval criticism of the Copernican theory concerning the fact that we cannot feel the Earth move under our feet.

12 Remember Arthur C. Clarke’s Third Law: “Any sufficiently advanced technology is indistinguishable from magic!”

13 Specifically, \(E(A, B) + E(A, B') + E(A', B) - E(A', B')\); for detail, please see Eqs. (1) and (2) from \cite{Popescu1994}.
hence quantum mechanics cannot be explained by a “classical theory” of the sort considered by Clauser, Horne, Shimony and Holt to derive their inequality. As demonstrated by Popescu and Rohrlich (1994), this combination can as large as 4 without violating weak locality, and indeed it is equal to 4 in our toy model of the world.

Have we uncovered a fundamental mistake in the paper of Clauser, Horne, Shimony and Holt? Not at all! Bell’s inequalities (including CHSH and those from Bell’s original 1964 paper) are proved, indeed correctly, under the assumption that the classical world is a theory of local hidden variables. The confusion comes from the fact that this has been widely misinterpreted to mean that quantum mechanics rules out any local realistic explanation of the world. For instance, Nielsen and Chuang (2000) wrote in their book: “These two assumptions together are known as the assumptions of local realism. […] The Bell inequalities show that at least one of these assumptions is not correct. […] Bell’s inequalities together with substantial experimental evidence now points to the conclusion that either or both of locality and realism must be dropped from our view of the world.” Note that Nielsen and Chuang consider here both locality and realism to be of the strong type, but our parallel lives mechanism is purely deterministic, hence it is strongly realistic as well.

The virtue of our toy model is to demonstrate in an exceedingly simple way that local realistic worlds can produce correlations that are demonstrably impossible in any classical theory based on local hidden variables. Therefore, it illustrates the importance of understanding the true meaning of Bell’s theorem. Nevertheless, it begs the question: what about quantum mechanics? Can it be explained in a local realistic parallel lives scenario?

It turns out that the idea of quantum mechanics being local and realistic in a theory analogous to parallel lives was discovered in the twentieth century: it can be traced back at least to Deutsch and Hayden (1999). Similar ideas were introduced subsequently by Rubin (2001) and Blaylock (2010). The article of Deutsch and Hayden focused on locality without precisely formulating definitions of realism or what we have called parallel lives, but their mathematical structure was quite similar to what we propose here. Of course, a complete reformulation of quantum mechanics along these lines is significantly more technical and complicated than what is needed to “explain” non-local boxes, but the conclusion is that the Church of the Larger Hilbert Space can be interpreted to provide a fully deterministic, strongly local and strongly realistic interpretation of quantum mechanics, Bell’s theorem notwithstanding. Indeed, this interpretation is not about parallel branches or parallel universes in a multiverse, but rather about parallel lives, which is a purely local phenomenon.

We are currently working on a followup article that will provide much more detail about our parallel lives theory.
Can Free Will Emerge from Determinism in Quantum Theory?

8 Free Will?

At this point, the fundamental question is “Can a purely deterministic quantum theory give rise to at least the illusion of nondeterminism, randomness, probabilities, and ultimately can free will emerge from such a theory”? Please note that this section is written at the first person as it reflects solely the opinion of the first author. The second author resolutely does not believe in free will and therefore his position is that neither determinism nor randomness would be able to enable it.

I cannot answer in a definitive way the question asked at the beginning of this section. Certainly, I acknowledge the difficulty of deriving the emergence of probabilities as mathematically inevitable from a quantum Universe in which all events occur unitarily according to the Church of the Larger Hilbert Space \cite{Kent2010}. However, we are faced with exactly the same difficulty if the collapse of the wave function does occur, or even in a purely classical world \cite{Duhamel2011}. I also acknowledge the difficulty of deriving free will from probabilities, randomness and nondeterminism. Nevertheless, I am inhabited by an unshakable belief that free will, if it exists, cannot have another origin, with apologies to the compatibilists.

In his own essay for our meeting, Gisin \cite{Gisin2012} expresses his view that the Many-World Interpretation of Quantum Mechanics “leaves no space for free will”. I suspect that he would have the same opinion concerning the Strong Church of the Larger Hilbert Space. [He also maintains that free will is not incompatible with the deterministic physics of Newton, but I fail to understand how classical physics could escape the “intelligence” of Laplace \cite{Laplace1814}, for which “nothing would be uncertain and the future, as the past, would be present to its eyes”.] In any case, I admit that Gisin may be right, but my most fundamental disagreement lies deeper than physics or mathematics when he says: “I enjoy free will much more than I know anything about physics”. I respect his opinion but my personal position is that I would prefer to live in a world without free will rather than in one in which the wavefunction collapses nonunitarily. After all, lack of free will in a deterministic universe does not deprive us from our capacity to experience surprise and find wonder in the world, because we cannot calculate, and hence predict, the future. But of course, whether or not free will exists, it does not extend to the point of letting each one of us choose in which of these two universes we actually live!

Perhaps cheap universes is our ultimate window on free will. Provided we firmly decide to follow whichever course of action it chooses for us, we are free to populate both branches of the Universal superposition. In whichever branch we perceive ourselves to be, we have made the free choice of letting quantum phenomena decide for us. Of course, I am not seriously suggesting that free will did not exist until the inception of cheap universes, just as Bell \cite{Bell1990} was not serious when he asked if “the wavefunction of the world [was] waiting to jump for thousands of millions of years until a single-celled living
creature appeared? Or did it have to wait a little longer, for some better qualified system… with a PhD?”!

9 Conclusion

In this essay, we have penned down for the first time our beliefs concerning the Universe in which we live, even though one of us (Brassard) has been inhabited by these thoughts for several decades. The more time goes by, the more convinced we are that they constitute the most rational explanation for our quantum world. We reject violently the notion that there would be a quantum-classical boundary and that physics is discontinuous, with a reversible (even unitary) evolution at the microscopic level but an irreversible collapse at the macroscopic level of measurements. It may be that free will can at best be an illusion in a world ruled by the Strong Church of the Larger Hilbert Space because every time you think that you make a decision (provided you use the services of cheap universes or some other source of true quantum randomness to make your choices), you also make the complementary decision in the Universal superposition. However, what does it matter if free will does not truly exist, provided the illusion is perfect?[14]

We give the last words of wisdom to Bell (1990), who ended his Summary of “Against ‘measurement’” by:

I mean […] by serious, that apparatus should not be separated off from the rest of the world into black boxes, as if it were not made of atoms and not ruled by quantum mechanics.

Perhaps it’s all nonsense, E pur si muove!

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We also benefitted from several crucial discussions with too many wonderful people to list them here even though they all helped shape our beliefs,

[14] Seriously, we would not want to live in the Matrix imagined by the Wachowski brothers, no matter how perfect is the simulation. So, perhaps we do care after all!
but we must mention at least Jeffrey Bub, Claude Crépeau, Patrick Hayden, Nicolas Gisin, Adrian Kent, Nathaniel David Mermin, the late Asher Peres and Alain Tapp. Even though G.B. has lived with these ideas for several decades, and many people throughout the years have asked him if he had anything written about it, who knows how much longer it would have been before he wrote them down, if ever, without the opportunity and motivation provided by Antoine Suarez and his 2010 meeting in Barcelona on *Is Science Compatible with Our Desire for Freedom?*

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[^15]: [http://www.socialtrendsinstitute.org/Activities/Bioethics/Is-Science-Compatible-with-Our-Desire-for-Freedom.axd](http://www.socialtrendsinstitute.org/Activities/Bioethics/Is-Science-Compatible-with-Our-Desire-for-Freedom.axd), accessed 29 February 2012.
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