Ionizing feedback from an O star formed in a shock-compressed layer

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ABSTRACT

We develop a simple analytical model for what happens when an O star (or compact cluster of OB stars) forms in a shock-compressed layer and carves out an approximately circular hole in the layer, at the waist of a bipolar H II region (HiR). The model is characterized by three parameters: the half-thickness of the undisturbed layer, \( Z_{\text{LAYER}} \), the mean number density of hydrogen molecules in the undisturbed layer, \( n_{\text{LAYER}} \), and the (collective) ionizing output of the star(s), \( \dot{N}_{\text{HeII}} \). The radius of the circular hole is given by \( W_{\text{circ}}(t) \sim 3.8 \text{ pc} \left[ Z_{\text{LAYER}}/0.1 \text{ pc} \right]^{-1/6} \left[ n_{\text{LAYER}}/10^4 \text{ cm}^{-3} \right]^{-1/3} \left[ \dot{N}_{\text{HeII}}/10^{49} \text{ s}^{-1} \right]^{1/6} \left[ t/\text{Myr} \right]^{2/3} \). Similar power-law expressions are obtained for the rate at which ionized gas is fed into the bipolar lobes, the rate at which molecular gas is swept up into a dense ring by the shock front that precedes the ionization front, and the density in this dense ring. We suggest that our model might be a useful zeroth-order representation of many observed HiRs. From viewing directions close to the mid-plane of the layer, the HiR will appear bipolar. From viewing directions approximately normal to the layer, it will appear to be a limb-brightened shell but too faint through the centre to be a spherically symmetric bubble. From intermediate viewing angles, more complicated morphologies can be expected.

Key words: hydrodynamics – stars: formation – ISM: bubbles – ISM: clouds – H II regions – ISM kinematics and dynamics.

1 INTRODUCTION

In Whitworth & Priestley (2021), we have derived an approximate analytical solution for the evolution of an H II region (HiR) excited by an O star or compact group of OB stars (hereafter, simply ‘the O star’) that has formed from a filament. This solution is applicable to the situation where the O star has formed at the end of a filament, due to the gravitational focusing that occurs there (e.g. Pon, Johnstone & Heitsch 2011; Pon et al. 2012; Clarke & Whitworth 2015), and also to the situation where the O star has formed at the confluence of a hub-and-spoke system of filaments (e.g. Peretto et al. 2013, 2014; Anderson et al. 2021), since each spoke filament will be eroded by the ionizing radiation from the O star more or less independently of the other spoke filaments.

Here, we consider the situation where the O star (again representing the case of a single O star or a compact cluster of OB stars) has formed near the centre of a shock-compressed molecular layer. For simplicity, we have in mind an approximately plane-parallel layer formed by the collision of two clouds or two converging flows (e.g. Elmegreen & Lada 1977; Elmegreen & Elmegreen 1978; Scoville, Sanders & Clemens 1986; Elmegreen 1994; Whitworth et al. 1994a,b; Tan 2000; Audit & Hennebelle 2005; Heitsch et al. 2006; Hennebelle & Audit 2007; Hennebelle, Audit & Miville-Duchênes 2007; Heitsch, Hartmann & Burkert 2008; Dale et al. 2009, 2011; Wünsch et al. 2010; Inoue & Fukui 2013; Chen & Ostriker 2014; Fukui et al. 2014; Takahira, Tasker & Habe 2014; Balfour et al. 2015; Chen & Ostriker 2015; Balfour, Whitworth & Hubber 2017; Dinnbier et al. 2017; Wu et al. 2017a,b; Inoue et al. 2018; Kohno et al. 2018; Shima et al. 2018; Takahira et al. 2018; Dobashi et al. 2019; Dobbs, Liow & Rieder 2020; Liow & Dobbs 2020; Tanvir & Dale 2020; Dobbs & Wurster 2021; Enokiya et al. 2021; Hayashi et al. 2021; Sakre et al. 2021).

Under this circumstance, the HiR excited by the O star expands most rapidly in directions approximately normal to the layer. In these directions, the ionization front (IF) may become density bounded, so that ionizing photons escape into the general interstellar medium. In directions close to the plane of the layer, expansion of the HiR proceeds more slowly, and the IF is preceded by a shock front (SF) that sweeps up the molecular gas in the layer into a dense ring (hereafter, the swept-up ring, SUR); this SUR may become sufficiently dense and massive to spawn a second generation of stars, i.e. a variant on the collect-and-collapse mechanism for propagating star formation (e.g. Whitworth et al. 1994a; Deharveng et al. 2003; Dale, Bonnell & Whitworth 2007; Thompson et al. 2012; Palmeirim et al. 2017). The ionized gas dispersing normal to, and on both sides of, the layer forms a bipolar HiR. The inside surface of the SUR appears as a bright rim and defines the waist of the bipolar HiR (e.g. Deharveng et al. 2015; Samal et al. 2018; Whitworth et al. 2018). Similar morphologies can be produced by mechanical feedback from winds and supernovae in layers (e.g. Wareing, Pittard & Falle 2017), and somewhat different configurations have been proposed for more violent cloud/cloud collisions (e.g. Ohama et al. 2018).

Viewed from directions close to the plane of the layer, both lobes of the bipolar HiR may be visible. Viewed from directions approximately normal to the layer, the bright rim will appear as a ring of enhanced emission. The standard interpretation of such rings of enhanced emission is that they represent the limb-brightened
projection of an approximately spherical HII region (e.g. Deharveng et al. 2010; Anderson et al. 2011; Li et al. 2020). However, there are some cases where the weak emission measure through the centre of the ring, and the low column density of molecular gas, is more compatible with a bipolar HII region breaking out of a layer (e.g. Beaumont & Williams 2010; Xu et al. 2017; Samal et al. 2018; Kabanovic et al. 2022). One example of an HII region that can be interpreted in this way is RCW 120 (e.g. Beaumont & Williams 2010; Anderson et al. 2015; Figueira et al. 2017), although alternative physical explanations have been proposed for this source, involving ionizing stars in turbulent clouds (Walch et al. 2015), and stellar-wind bubbles (Mackey et al. 2016) or HII bubbles (Marsh & Whittow 2019) due to stars that are moving supersonically relative to the ambient molecular gas. Other examples of partial or total ring-like morphologies include the shell round λ Orionis (Lee, Seon & Jo 2015) and G35.673-00.847 (Dewangan, Devaraj & Ojha 2018).

The plan of the paper is as follows: In Section 2, we define a simple geometric model for the configuration. We introduce the three configuration parameters \( Z_{\text{layer}}, n_{\text{layer}}, \mathcal{N}_{\text{HII}} \) that define a particular realization of the model and the four ansätze that allow us to simplify the dynamical equations. In Section 3, we formulate the equation of ionization balance in the HII region, between the O star and the IF on the inside of the SUR. In Section 4, we derive approximate expressions for the density and sound speed in the SUR and the bulk velocity of the SUR. In Section 5, we obtain a differential equation for the position of the IF, a numerical solution to this equation, and an approximate analytical solution. In Section 6, we obtain an approximate analytical expression for the rate at which ionized gas boils off the IF and escapes into the bipolar lobes. In Section 7, we obtain a differential equation for the growth of the SUR, a numerical solution to this equation, and an approximate analytical solution. In Section 8, we review the assumptions and approximations made, and attempt to identify those that might alter the results significantly. In Section 9, we discuss the results, and in Section 10 we summarize the main results.

The essential difference between the situation considered here (a ring-shaped IF eroding a circular hole in a plane-parallel layer) and the situation considered in the earlier paper (Whittworth & Priestley 2021; a hemispherical IF eroding the end of a cylindrical filament) is the geometry. Whereas the filament presents a rather small solid angle to the O star, and one that decreases rather fast \([L^{-2}(t)\text{, where } L^{-2}(t) = \text{the distance from the O star to the IF where it eats into the end of the filament, the layer presents a larger solid angle to the O star, and one that decreases more slowly as } W_{\text{mol}}^{-1}(t)\text{, where } W_{\text{mol}}^{-1}(t) = \text{the distance from the O star to the IF where it eats into the layer}]. Consequently, at late times the O star releases much more ionized gas from the layer, and sweeps up much more neutral gas into the SUR, in the situation analysed here – than in the situation analysed by Whittworth & Priestley (2021), where much less ionized gas is released from the end of the filament, and much less neutral gas is swept between the IF and the SF.

2 MODEL

In this section, we define the geometry of the model, introduce the three dimensionless parameters that specify a particular configuration \( Z_{\text{HII}}, n_{\text{HII}}, \mathcal{N}_{\text{HII}} \), and introduce the approximations and assumptions that underlie the subsequent analysis. Most of these approximations and assumptions are evaluated retrospectively in Section 8.

We model the undisturbed layer as a semi-infinite homogeneous slab, with reflection symmetry about the \( z = 0 \) plane (see Fig. 1). The layer has half-thickness \( Z_{\text{layer}} \), i.e. it is confined to \( |z| < Z_{\text{layer}} \), and we define a dimensionless half-thickness \( Z_{\text{HII}} = Z_{\text{layer}} / \langle 0.1 \text{ pc} \rangle \).

The gas has solar composition \([X = 0.70, Y = 0.28, Z = 0.02] \), and we assume that in the layer all the hydrogen is molecular. The mean mass associated with each hydrogen molecule, when contributions from all other elements, in particular helium, have been taken into account, is therefore \( \bar{m}_H = 2m_H/X = 4.75 \times 10^{-24} \text{ g} \), where \( m_H \) is the mass of a hydrogen atom.

In the undisturbed layer, the number density of molecular hydrogen is \( n_{\text{HII}} \), and we define a dimensionless number density \( n_{\text{HII}} = n_{\text{HII}} / \langle 10^4 \text{ cm}^{-3} \rangle \).

It follows that the surface density of the layer is

\[
\Sigma_{\text{layer}} = 2 Z_{\text{layer}} n_{\text{HII}} \bar{m}_H
\]

\[
= 140 M_\odot \text{ pc}^{-2} Z_{\text{HII}} n_{\text{HII}}
\]

\[
= 6.2 \times 10^{31} \text{ H}_2 \text{ cm}^{-2} Z_{\text{HII}} n_{\text{HII}}.
\]

We assume that the layer is sufficiently massive that it is marginally unstable against break-up. Hence, the effective sound speed in the layer (due to thermal and turbulent motions) is

\[
c_{\text{layer}} = \left\{ \pi G Z_{\text{layer}}^2 n_{\text{HII}} \bar{m}_H \right\}^{1/2}
\]

\[
= 0.31 \text{ km s}^{-1} Z_{\text{HII}} n_{\text{HII}}^{1/2}.
\]

We also assume that the O star has formed at the centre of the layer, \([x, y, z] = [0, 0, 0] \), and does not move (we review this assumption in Section 8.1). At time \( t = 0 \), the O star starts to emit ionizing photons at a constant rate \( \mathcal{N}_{\text{HII}} \) (we review this assumption in Section 8.2), and we define a dimensionless ionizing output,

\[
\mathcal{N}_{\text{HII}} = \mathcal{N}_{\text{HII}} / \langle 10^{49} \text{ s}^{-1} \rangle.
\]

A circular IF (implicitly a hydrogen-ionization front) propagates outwards from the O star, creating a circular hole in the molecular layer, which is filled by the HII region.

In our model, the three dimensionless parameters, \( Z_{\text{HII}}, n_{\text{HII}}, \mathcal{N}_{\text{HII}} \) (equations 1, 2, and 8), are the only parameters influencing the evolution of the HII region. They feature in many of the subsequent equations. All the variables used in the analysis, along with the acronyms, are summarized in Table 1.

The ionized gas in the HII region disperses due to both the momentum with which this gas boils off the IF and its high thermal pressure. We assume that the ionized gas has uniform and constant gas-kinetic temperature, \( T_\text{HII} = 10^4 \text{ K} \), hence uniform and constant adiabatic sound speed, \( c_s = 15 \text{ km s}^{-1} \), and uniform and constant Case B recombination coefficient, \( a_{\text{HII}} = 2.7 \times 10^{-13} \text{ cm}^3 \text{ s}^{-1} \). We neglect the ionization of helium. The assumption of uniform and constant temperature, and the neglect of helium ionization, is reasonable because we shall be mainly concerned with the ionized gas near the IF. Here, the ionizing radiation is rather hard, and likely to maintain a high gas-kinetic temperature, \( T_\text{HII} \sim 10^4 \text{ K} \). Moreover, unless the mean effective temperature of the O star is exceptionally high, no...
Figure 1. Cartoon illustrating the geometry of the model on the \([w, z]\) plane. The configuration has cylindrical symmetry about the \(z\)-axis and reflection symmetry about the \(z = 0\) plane; \(w = [x^2 + y^2]^{1/2}\). The O star sits at the origin \([w, z] = [0, 0]\). The bold outline on the right represents the boundary of the ‘molecular layer’, which is characterized by half-thickness, \(Z_{\text{layer}}\), molecular hydrogen density, \(n_{\text{layer}}\), and effective sound speed, \(c_{\text{layer}}\). In the direction towards the O star, the molecular gas of the layer terminates in a semicircular IF, at distance \(W_0(t)\) from the O star. As the IF advances into the layer, it is preceded by an SF, at distance \(W_0(t)\) from the O star. Between the IF and the SF is a dense ring of swept-up molecular gas, represented by the thick black meniscus shape, and labelled ‘SWEPT-UP RING’ (SUR), with molecular hydrogen density \(n_{\text{SUR}}(t)\) and effective sound speed \(c_{\text{SUR}}\). The HIR between the O star and the IF is characterized by recombination coefficient, \(\alpha_0\), adiabatic sound speed, \(c_{\text{SF}}\), and proton density, \(n_p(r, t)\). Here, \(r\) is the distance from the COC of the IF. The ionized gas flowing off the IF disperses as indicated by the curved ‘FLOW-LINES’, to produce a bipolar HIR, with the SWEPT-UP RING defining its waist.

helium-ionizing photons will reach that far; i.e. the helium IFs will be closer to the O star.

As the IF propagates outwards into the layer, it is preceded by an SF, which sweeps up the neutral gas of the layer. The passage of the SF will probably not change the gas-kinetic temperature much, but it is likely to amplify the turbulent motions, so that the effective sound speed in the SUR is increased somewhat. As in Whitworth & Priesty (2021), we assume that \(c_{\text{SUR}} \approx 2^{1/2} c_{\text{layer}}\) (see equations 6 and 28); in other words, the amount of turbulent energy is approximately doubled on passing through the shock. This assumption cannot be justified precisely, but appears to be a good approximation to the amplification of turbulence behind accretion shocks, and does not affect the results significantly.\(^2\)

The model is concerned with (i) the dynamics of the dispersing ionized gas, (ii) the consequent advance of the IF, and (iii) the sweeping up of neutral gas immediately ahead of the IF. At the heart of the model are the following four ansätze.

\textit{Ansatz 1.} The HIR and the SUR have reflection symmetry about the \(z = 0\) plane and cylindrical symmetry about the \(z\)-axis (see Fig. 1). Hence, we can switch to cylindrical polar coordinates \([w, \phi, z]\), so that all quantities only depend on \(w = [x^2 + y^2]^{1/2}\) and \([z]\), and are independent of \(\phi = \tan^{-1}(y/x)\). For brevity, we will refer to the circle defined by \([w, 0 \leq \phi < 2\pi, z]\) as ‘a point’ with coordinates \([w, z]\).

\textit{Ansatz 2.} Ionized gas flowing radially off the IF diverges, and so the recombination rate decreases with distance from the IF. This divergence is largely determined by the curvature of the IF, which is of order \(Z_{\text{layer}}^{-1}\). We can then compute the position of the IF by integrating the rate of recombination along the \(w\)-axis from the O star to the closest point on the IF at \([w, z] = [W_0(t), 0]\) (see equation 17).

\textit{Ansatz 3.} Ionized gas flows off each point on the IF at the same rate, and this rate can be approximated by the rate at \([w, z] = [W_0(t), 0]\) (computed as described in \textit{ansatz} 2 and Section 3). Evidently, this overestimates the flow rate off all other points on the IF, by a factor that increases with \([z]\), in particular because ionizing radiation arrives at these points at an increasingly oblique angle to the IF as we move away from the \(z = 0\) plane. We compensate for this by assuming that the area of the IF is only \(\sim 4\pi W_0(t) + Z_{\text{layer}}^2\) (the projected cross-sectional area of the IF as seen from the O star) rather than the full \(\sim 2\pi^2 W_0(t) + Z_{\text{layer}}^2\) (the area of the convex inner surface of the SUR).

\textit{Ansatz 4.} If the gas were to flow radially off the IF to infinity, it would converge on the \(z\)-axis to produce a singularity in the volume density. We neglect this convergence, since radiation pressure and/or winds from the O star deflect the ionized gas outwards and away from the O star. We only take account of the divergence in the vicinity of the IF (see Fig. 1), which is where most of the ionizing radiation emitted in these directions is absorbed – as evidenced by the brightness of ‘bright rims’.

\(^2\)Whitworth & Jaffe (2018) show that molecular-line cooling effectively reduces post-shock velocities to transonic values, but the cooling then stalls due to saturation of the cooling lines. If we assume that this factor also applies to the non-thermal velocity dispersion, then the post-shock velocity dispersion should be roughly twice the pre-shock value.
Table 1. Definitions of acronyms and mathematical symbols.

| Acronyms                        | Definition                                                                 |
|--------------------------------|---------------------------------------------------------------------------|
| H ii region                    | HiR                                                                       |
| Ionization front               | IF                                                                        |
| Centre of curvature of IF      | COC                                                                      |
| Shock front                    | SF                                                                       |
| Swept-up ring                  | SUR                                                                      |

Configuration parameters and fiducial values

| Half-thickness of layer         | $Z_{\text{layer}}$                                                       |
| Density of H$_2$ in layer       | $n_{\text{H}_2}^{\text{layer}}$                                         |
| Output of ionizing photons      | $N_{\text{ion}}$                                                        |
| Effective sound speed in layer  | $c_{\text{layer}}$                                                      |
| Effective sound speed in SUR    | $c_{\text{SUR}}$                                                        |

Fixed parameters and values

| Temperature in ionized gas      | $T_\text{b}$ = $10^4$ K                                                 |
| Sound speed in ionized gas      | $c_\text{b}$ = 15 km s$^{-1}$                                           |
| Case B recombination coeff.     | $\alpha_\text{b}$ = $2.7 \times 10^{-13}$ cm$^3$ s$^{-1}$               |

Dependent variables

| Distance from O star to IF      | $W_\text{IF}(t)$                                                        |
| Distance from O star to SF      | $W_\text{SF}(t)$                                                        |
| Thickness of SUR                | $\Delta W_{\text{SUR}}(t)$                                              |
| Density of protons at IF        | $n_{\text{p}}(t)$                                                      |
| Density of protons in HiR       | $n_{\text{p}}(\text{HiR}, t)$                                           |
| Density of H$_2$ in SUR          | $n_{\text{H}_2}(t)$                                                   |
| Bulk velocity in SUR            | $v_{\text{SUR}}(t)$                                                    |
| Mass of SUR                     | $M_{\text{SUR}}(t)$                                                    |

Independent variables

| Time since O star switch-on     | $t$                                                                      |
| Radial distance from CO          | $r$                                                                     |
| Distance along symmetry axis     | $z$                                                                     |
| Distance from symmetry axis      | $w$                                                                     |

Dimensionless variables

| Dimensionless $t$ | $\tau$ | $\xi_{\text{SUR}}(r,t)$ | $\xi_{\text{IF}}(t)$ | $W_\text{IF}(t)/Z_{\text{layer}}$ | $W_\text{SF}(t)/Z_{\text{layer}}$ | $\delta_{\text{SUR}}(r,t)$ | $\Delta W_{\text{SUR}}(t)/Z_{\text{layer}}$ |

With these ansätze, the location of the IF is given by

$$z_{\text{IF}}(w, t) \approx \left\{ Z_{\text{IF}}^2 + \left[ W_\text{IF}(t) + Z_{\text{layer}} - w \right]^2 \right\}^{1/2}$$

$$W_\text{IF}(t) < w < W_\text{IF}(t) + \left[ 1 - \cos(1) \right] Z_{\text{layer}}$$

where $\cos(1) = 0.5403$.

The point on the SF closest to the O star is at $[w, z] = [W_\text{SF}(t), 0]$. Hence, the thickness of the SUR, measured parallel to the $w$-axis, is

$$\Delta W_{\text{SUR}}(t) \approx W_\text{SF}(t) - W_\text{IF}(t)$$

and the locus of the shock is

$$z_{\text{IF}}(w, t) \approx z_{\text{IF}}(w - \Delta W_{\text{SUR}}(t), t)$$

In general, $\Delta W_{\text{SUR}}(t) \ll W_\text{IF}(t)$; in other words, the SUR is quite thin, radially. This is demonstrated retrospectively in Section 8.3. Hence, $W_\text{IF}(t) \approx W_\text{IF}(t)$.

Our model does not involve a magnetic field. We speculate on the consequences of including a magnetic field in Section 8.7.

3 ionization balance

In this section, we formulate the condition of ionization balance in the space between the O star and the IF.

For the sake of simplicity, we exploit the fact that there is an extremely short period when the gas has not had time to move far,

and many of the ionizing photons are being expended ionizing gas for the first time. This period is very short, of order a few (say 10) recombination times,

$$0 < t \lesssim \frac{5}{\alpha_\text{b}(T) n_{\text{layer}}^{\text{SUR}}} \sim 0.00606 \text{ Myr} n_3^{-1}$$

After this, there is a period during which the IF is R-type (Kahn 1954), but this too is relatively short-lived. Thereafter, the IF switches to being D-critical (Kahn 1954), and most of the ionizing radiation is expended maintaining ionization against recombination in the region between the O star and the IF. Only a small fraction of the ionizing radiation gets to ionize new material at the advancing IF (we check this retrospectively in Section 8.4). The newly ionized gas is significantly overpressured, and therefore rapidly expands away from the IF.

Ionized gas flows off the D-critical IF at the adiabatic sound speed, $c_\text{a}$, and we assume that the volume density in the ionized gas decreases approximately as $[r/Z_{\text{layer}}]^{-1}$, where $r$ is the distance from the centre of curvature (COC) of the IF,

$$r = \left\{ \left[ W_\text{IF}(t) + Z_{\text{layer}} - w \right]^2 + z^2 \right\}^{1/2}$$

and the COC is at $[w, z] = [W_\text{IF}(t) + Z_{\text{layer}}, 0]$ (see Fig. 1). In other words, we neglect acceleration of the flow of ionized gas, as it flows away from the IF. This will reduce the recombination rate further, but will not greatly affect the advance of the IF, because the attenuation of the ionizing flux is dominated by the dense region near the IF, as evident in equation (16).

Since we are assuming that the O star is not sufficiently hot to ionize helium all the way to the IF, the volume density of protons in the vicinity of the IF is the same as the volume density of electrons, and we approximate this by

$$n_{\text{H}}(r, t) = n_\text{b}(t) \left[ r/Z_{\text{layer}} \right]^{-1}$$

i.e. we separate the time dependence from the radial dependence. This is an acceptable approximation, provided that the time-scale on which the IF advances is much longer than the time-scale on which ionized gas streams far away from the IF. We show that this is indeed the case in Section 8.5.

The recombination rate per unit volume is therefore

$$R(r, t) = \alpha_\text{b} n_{\text{H}}^2(r, t) \approx \alpha_\text{b} n_\text{b}^2(t) \left[ r/Z_{\text{layer}} \right]^{-2}$$

Here, $n_{\text{IF}}(t)$ is the volume density of protons immediately outside the IF. In Section 6, we obtain a closed expression for $n_{\text{IF}}(t)$ (equation 48).

On the $w$-axis ($z = 0$), and in the HiR $[w < W_\text{IF}(t)]$, we have $r = W_\text{IF}(t) + Z_{\text{layer}} - w$. Therefore, if we (a) neglect the small fraction of ionizing photons that reach the IF and ionize new material, and (b) equate the supply of ionizing photons to the rate of recombination integrated along the $w$-axis from the O star to the IF, ionization balance requires

$$N_{\text{IFC}} \approx \int_{w=0}^{[W_\text{IF}(t) + 2 Z_{\text{layer}}]} \alpha_\text{b} n_{\text{b}}^2(t) Z_{\text{layer}}^2 4\pi w^2 dw$$

$$\approx 4\pi \alpha_\text{b} n_{\text{b}}^2(t) Z_{\text{layer}}^2 \left\{ \left[ W_\text{IF}(t) + Z_{\text{layer}} \right]^2 - w^2 \right\}$$

$$-2 \left[ W_\text{IF}(t) + Z_{\text{layer}} \right] \ln \left[ \frac{W_\text{IF}(t) + Z_{\text{layer}}}{Z_{\text{layer}}} \right]$$. (17)

This is a key equation relating the two time-dependent quantities, $n_{\text{IF}}(t)$ and $W_\text{IF}(t)$, to the configuration parameters, $N_{\text{IFC}}$ and $Z_{\text{layer}}$.
4 STRUCTURE OF THE SHOCK-COMPRESSED LAYER

The volume density of molecular hydrogen in the SUR is
\[ n_{\text{SUR}}(t) \approx n_{\text{LAYER}} \left( \frac{dW_{\text{SF}}}{dt} \right)^2 \left( \frac{c_{\text{SUR}}}{c_{\text{LAYER}}} \right)^2, \]  
(18)
due to compression where the undisturbed gas in the layer is swept up into the SUR, and conservation of mass across the SF requires
\[ n_{\text{LAYER}} \frac{dW_{\text{SF}}}{dt} \approx n_{\text{SUR}}(t) \left( \frac{dW_{\text{SF}}}{dt} - v_{\text{SUR}}(t) \right), \]  
(19)
where \( v_{\text{SUR}}(t) \) is the velocity of the shock-compressed gas, parallel to the \( w \)-axis. Eliminating \( n_{\text{SUR}}(t) \) between equations (18) and (19), we obtain
\[ v_{\text{SUR}}(t) \approx dW_{\text{SF}}/dt - \frac{c_{\text{SUR}}^2}{dW_{\text{SF}}/dt}. \]  
(20)

As shown in the appendix to Whitworth & Priestley (2021), gas flows into the D-critical IF at speed \( c_w \), and hence
\[ dW_{\text{SF}}/dt - v_{\text{SUR}}(t) \approx c_w^2/2c_w. \]  
(21)

Ionized gas flows off the D-critical IF at speed \( c_w \), so conservation of mass across the IF gives
\[ n_{\text{SUR}}(t) \approx n_w(t) \left[ c_w/c_{\text{SUR}} \right]^2. \]  
(22)

Eliminating \( n_{\text{SUR}}(t) \) between equations (18) and (22), we obtain
\[ dW_{\text{SF}}/dt \approx c_w \left[ n_w(t)/n_{\text{LAYER}} \right]^{1/2}. \]  
(23)

If we now define the dimensionless parameter
\[ \chi(t) = \left( \frac{n_{\text{SUR}}(t)}{n_{\text{LAYER}}} \right)^{1/2} \approx \frac{c_w}{c_{\text{SUR}}} \left[ \frac{n_w(t)}{n_{\text{LAYER}}} \right]^{1/2}, \]  
(24)
equation (23) becomes
\[ dW_{\text{SF}}/dt \approx c_{\text{SUR}} \chi(t). \]  
(25)

Combining equations (20) and (21),
\[ \frac{dW_{\text{SF}}}{dt} = \frac{dW_{\text{SF}}}{dt} - \frac{c_{\text{SUR}}^2}{2c_w} \approx \frac{c_{\text{SUR}}^2}{2c_w} \chi(t) - \frac{1}{\chi(t)}, \]  
(27)
where to obtain the final expression (equation 27), we have dropped the third term \( c_{\text{SUR}}^2/2c_w \) in the expression on the preceding line (equation 26). We justify this in Section 8.6.

From equation (6),
\[ c_{\text{SUR}} = \left\{ 2\pi G Z_{\text{LAYER}}^2 n_{\text{LAYER}} \rho_{H_2} \right\}^{1/2} \]  
(28)
\[ = 0.44 \text{ km s}^{-1} Z_{\text{o.s.i.}} n_{1/2}^{1/2}, \]  
(29)
from equations (10), (25), and (26),
\[ \frac{d\Delta W_{\text{SUR}}}{dt} = \frac{dW_{\text{SF}}}{dt} - \frac{dW_{\text{IF}}}{dt} \approx \frac{c_{\text{SUR}}}{\chi(t)}; \]  
(30)
and from equations (18) and (25),
\[ n_{\text{SUR}}(t) \approx n_{\text{LAYER}} \chi^2(t). \]  
(31)

5 ADVANCE OF THE IONIZATION FRONT

In this section, we derive and solve an equation for the advance of the IF.

We first introduce the dimensionless parameter
\[ K = \frac{2\pi}{2} \left[ G m_{H_2} \right]^{1/2} Z_{\text{LAYER}}^2 n_{\text{LAYER}} \left[ \frac{\pi N_{\text{LyC}} Z_{\text{LAYER}}}{\alpha_p} \right]^{1/4} \]  
(32)
\[ \approx 34 Z_{\text{o.s.i.}}^{-1/4} n_{1/2}^{-1/4} N_{\text{LyC}}^{1/4}, \]  
(33)
which measures the speed at which the O star erodes the layer, and the dimensionless length and time variables,
\[ \tau = \frac{c_{\text{SUR}}}{Z_{\text{LAYER}}}, \]  
(34)
\[ \xi_w(\tau) = \frac{W_w(t)}{Z_{\text{LAYER}}}, \]  
(35)
\[ \xi_{\text{IF}}(\tau) = \frac{W_{\text{IF}}(t)}{Z_{\text{LAYER}}}, \]  
(36)
\[ \Delta \xi_{\text{SUR}}(\tau) = \frac{W_{\text{SF}}(t)}{Z_{\text{LAYER}}}. \]  
(37)

\( n_w(t) \) can then be eliminated between equations (17) and (24). Equations (26), (28), and (32) are then combined to give
\[ \frac{d\xi_w}{d\tau} \approx \chi(\tau) - \frac{1}{\chi(\tau)}, \]  
(38)
\[ \chi(\tau) = K \left\{ \xi_w(\tau)^2 + 2\xi_{\text{IF}}(\tau) - 2(1 + \xi_{\text{IF}}(\tau)) \ln (1 + \xi_{\text{IF}}(\tau)) \right\}^{1/2}, \]  
(39)
Equations (38) and (39) are the equations of motion for the IF, and must be solved numerically.

We start the integration of equation (38) with \( W_w(t) \) equal to the Strömgren radius at the density in the layer,
\[ W_w(0) = R_{\text{STROMGREN}} = \left[ \frac{3 N_{\text{LyC}} Z_{\text{LAYER}}}{4 \pi \alpha_p n_{\text{LAYER}}} \right]^{1/3}, \]  
(40)
and hence
\[ \xi_w(0) \rightarrow = 1.44 Z_{\text{o.s.i.}}^{-1} n_{1/2}^{-2/3} N_{\text{LyC}}^{-1/3}. \]  
(41)

but note that this choice does not affect the subsequent evolution significantly.

Accurate numerical solutions for \( \xi_{\text{IF}}(\tau) \), obtained by integrating equations (38) and (39), with initial conditions given by equation (41), are plotted with full lines in Fig. 2, for five representative values of \( K \), distributed about the fiducial value computed in equation (32), viz. 17.0, 24.0, 34.0, 48.1, and 68.0. As expected, the IF advances faster for larger values of \( K \), i.e. if the layer is geometrically thinner and/or less dense, and/or the ionizing output of the O star is larger.

We can also obtain an approximate asymptotic solution by considering the limit \( \xi_{\text{IF}}(\tau) \gg 1 \). Equations (38) and (39) then yield
\[ \frac{d\xi_{\text{IF}}}{d\tau} = \frac{K}{\xi_{\text{IF}}^2(\tau)} \]  
(42)
\[ \chi(\tau) \sim \left[ 2 K^2 / 3 \right]^{1/3}, \]  
(43)
\[ \sim 5.5 Z_{\text{o.s.i.}}^{-7/6} n_{1/2}^{-5/6} N_{\text{LyC}}^{-1/6} t / \text{Myr}^{-1/3}. \]  
(44)

The approximate asymptotic solution (equation 42) is plotted with dashed lines on Fig. 2, for the same five values of \( K \). There is very close agreement between the accurate numerical solution and the approximate asymptotic solution. Since the latter is analytical, we use it in the sequel to estimate other properties of the HiR and the SUR. Again, we note that the advance is faster if the layer is geometrically thinner, and/or the layer is less dense, and/or the ionizing output.
of the O star is larger; the dependence on the ionizing output is, however, quite weak.

Converting equation (42) back to physical variables, we obtain

\[ W_w(t) \sim 3.8 \text{ pc} \frac{Z_{01}}{n_4} n_4^{-1/3} \frac{N_1^{1/6}}{40^3} \left[ \tau/\text{Myr} \right]^{1/3}, \]

(45)

\[ t(W_w) \sim 0.135 \text{ Myr} \frac{Z_{01}}{n_4} n_4^{1/2} \frac{N_1^{-1/4}}{40^3} \left[ W_w/\text{pc} \right]^{3/2}, \]

(46)

\[ dW_w/d\tau \sim 2.3 \text{ km s}^{-1} \frac{Z_{01}}{n_4} n_4^{-1/3} \frac{N_1^{1/6}}{40^3} \left[ \tau/\text{Myr} \right]^{-1/3}. \]

(47)

6 DYNAMICS OF THE OVERALL H II REGION

In this section, we solve for the rate at which ionized gas boils off the IF, and hence for the total mass of H II released from the filament by the O star.

From equation (24), the density of ionized gas at the IF is

\[ n_{\text{sur}}(t) \approx n_{\text{layer}} \frac{c_{\text{sur}} Z(t)}{c_0} \]

\[ \sim 270 \text{ cm}^{-3} \frac{Z_{01}}{n_4} n_4^{-1/3} \frac{N_1^{1/6}}{40^3} \left[ \tau/\text{Myr} \right]^{-2/3}. \]

(48)

Strictly speaking, the expressions and estimates derived thus far (equations 16 through 49) pertain only to the gas on the z-axis. The flux of ionizing radiation incident on other parts of the IF decreases with distance from the w-axis, largely because it arrives at increasingly oblique angles. To take account of this, we invoke the third of the ansätze defined in Section 2, i.e. we assume that the expressions and estimates derived thus far obtain everywhere, not just on the w-axis, and to compensate for this we limit the area of the IF to the cross-sectional area of the layer as seen from the O star, 

\[ \approx 4\pi [W_w(t) + Z_{\text{layer}}] Z_{\text{layer}} \sim 4\pi W_w(t) Z_{\text{layer}}. \]

The net rate at which ionized gas flows off the IF is therefore

\[ dM_w/d\tau \sim \pi W_w(t) Z_{\text{layer}} n_{\text{sur}}(t) m_{H_2} c_w \]

\[ \sim 350 M_\odot \text{ Myr}^{-1} Z_{01}^{-1/2} N_1^{1/2}, \]

(50)

\[ \text{and the total mass boiled off the IF is} \]

\[ M_w(t) \sim 350 M_\odot Z_{01}^{1/2} N_1^{1/2} [\tau/\text{Myr}]. \]

(51)

As we show below (Section 7), this is quite a modest mass, as compared with the mass that is swept up into the SUR.

7 GROWTH OF THE SHOCK-COMPRRESSED RING

In this section, we derive the parameters of the SUR (thickness, mass, and expansion velocity).

The thickness of the SUR grows at a rate given by equation (30), and hence in terms of dimensionless variables,

\[ \frac{d\Delta \xi_{\text{SUR}}}{d\tau} \approx \frac{1}{\chi(t)}. \]

(53)

Accurate numerical solutions for \( \Delta \xi_{\text{SUR}}(t) \) obtained by integrating equation (53) with \( \chi(t) \) from equation (43), the initial condition \( \Delta \xi_{\text{SUR}}(0) = 0 \), and \( K = 17.0 \), 24.0, 34.0, 48.1, and 68.0, are plotted with full lines in Fig. 3.

In the limit that \( \xi_{\text{sur}}(t) \gg 1 \), we can substitute for \( \chi(t) \) in equation (53) from equation (43) to obtain

\[ \frac{d\Delta \xi_{\text{SUR}}}{d\tau} \sim \frac{3 \tau}{2 K^2}. \]

(54)

and hence an approximate analytical solution,

\[ \Delta \xi_{\text{SUR}}(t) \sim \left[ 81 \tau^2 / 128 K^2 \right]^{1/3}. \]

(55)

The approximate asymptotic solution (equation 55) is plotted with dashed lines on Fig. 3, for the same five values of \( K \). Again there is very good agreement between the accurate numerical solution and the approximate asymptotic solution, and we adopt the latter because it is analytical. Converting back to physical variables, equation (55) gives

\[ \Delta W_{\text{SUR}}(t) \sim 0.06 \text{ pc} Z_{01}^{1/3} n_4^{4/3} N_1^{-1/6} [\tau/\text{Myr}]^{1/3}. \]

(56)

The density in the SUR is given by equation (31),

\[ n_{\text{sur}}(t) \sim 3.1 \times 10^5 \text{ H}_2 \text{ cm}^{-3} Z_{01}^{-3/2} n_4^{-2/3} N_1^{1/3} [\tau/\text{Myr}]^{-2/3}. \]

(57)

The total mass swept up by the SF is given by

\[ M_{\text{SUR}}(t) \sim \pi W_{\text{w}}(t) Z_{\text{layer}} \]

\[ \sim 6400 M_\odot Z_{01}^{1/2} n_4^{-1/3} N_1^{1/3} [\tau/\text{Myr}]^{1/3}. \]

(58)

Comparing this with the total mass boiled off the IF (equation 52), we see that, if we adopt the fiducial parameters, then at late times
8.4 Fraction of ionizing photons reaching the IF

In deriving equation (16), which constrains the position of the IF by requiring a balance between ionization and recombination on the line from the O star to the IF, we have ignored the ionizing photons that reach the IF and ionize new material. Since ionized gas flows off the IF at speed $c_{\text{if}}$, the number flux of hydrogen-ionizing photons impinging on the IF is given by $n_{\text{if}}(t) c_{\text{if}}$. The number flux of ionizing photons that would impinge on the IF if there were no absorption (to balance recombination) in the region between the O star and the IF is $\dot{N}_{\text{if,c}}/4\pi W_{\text{IF}}(t)$. Thus, the fraction of ionizing radiation expended producing new ionizations at the IF is

$$\frac{n_{\text{if}}(t) c_{\text{if}}}{\dot{N}_{\text{if,c}}/4\pi W_{\text{IF}}(t)} = 0.07 Z_{\text{if}}^{1/2} n_{\text{if}}^{3/2} \dot{N}_{\text{if,c}}^{1/2} [t/\text{Myr}]^{-2/3}.$$  (63)

This fraction is small and remains small ($\leq 0.20$) for $t \lesssim 5$ Myr, so we are justified in neglecting it in deriving equation (16).

8.5 Separation of variables

In deriving equation (14), we have split the $r$-dependence of $n_{\text{if}}(r, t)$ from the $t$-dependence. This split is acceptable provided that the IF advances on a time-scale much longer than the time-scale it takes for newly ionized gas to get far from the IF, which reduces to the condition

$$W_{\text{IF}}(t) \frac{\text{d}W_{\text{IF}}}{\text{d}t} \gg \frac{Z_{\text{layer}}}{c_{\text{if}}}.$$  (64)

Substituting from equations (45) and (47), the time-scale on which the IF advances is

$$W_{\text{IF}}(t) \frac{\text{d}W_{\text{IF}}}{\text{d}t} \sim 1.65 \text{ Myr}.$$  (65)

The time-scale on which ionized gas flows away from the IF is

$$\frac{Z_{\text{layer}}}{c_{\text{if}}} \sim 0.0065 \text{ Myr} Z_{\text{if}}.$$  (66)

Evidently, separation of the $r$-dependence from the $t$-dependence is justified.

8.6 Speed of SF

In deriving equation (27) from equation (26), we have dropped the term $-c_{\text{if}}^2/2c_{\text{if}}$, on the assumption that $dW_{\text{SF}}/dt \ll 2c_{\text{if}}$. Since $dW_{\text{SF}}/dt \simeq dW_{\text{IF}}/dt$, equation (47) gives

$$dW_{\text{SF}}/dt \sim 2.3 \text{ km s}^{-1} Z_{\text{if}}^{-1/6} n_{\text{if}}^{-1/3} \dot{N}_{\text{if,c}}^{1/6} [t/\text{Myr}]^{-1/3}.$$  (67)

Evidently, $dW_{\text{SF}}/dt \ll 2c_{\text{if}} \approx 30 \text{ km s}^{-1}$, except at very early times where the analysis presented here is not expected to apply (see the discussion at the start of Section 3).

Having placed an upper limit on the speed of the SF, we should also check that the SF advances sufficiently fast to compress the gas it sweeps up. Comparing $dW_{\text{SF}}/dt$ from equation (67), with $c_{\text{if}}$ from equation (29), we see that there will only be a shock if the layer is not too thick and not too dense, and the ionizing output is not too small.

8.7 Neglect of magnetic field

Since observations (e.g. Ward-Thompson et al. 2017; Fissel et al. 2019; Soam et al. 2019; Pillai et al. 2020; Doi et al. 2020; Arzoumanian et al. 2021; Kwon et al. 2022; Pattle et al. 2022) and simulations (e.g. Soler et al. 2013; Seifried & Walch 2015; Girichidis et al. 2018;
Gómez, Vázquez-Semadeni & Zamora-Avilés (2018) suggest that the gas flows assembling dense star-forming gas structures tend to involve velocities parallel or antiparallel to the large-scale magnetic field, we limit discussion to a large-scale magnetic field parallel to the z-axis. In this situation, there are two effects that should be considered. First, the field will inhibit gravitational fragmentation of the layer (see Section 8.7.1). Secondly, the field will resist the advance of the IF (see Section 8.7.2). We note that large-scale magnetic fields in the interstellar medium are typically \( \lesssim 10 \, \mu \text{G} \) (e.g. Heiles & Troland 2005).

### 8.7.1 Stability of the layer against gravitational fragmentation

If the undisturbed field is \( \mathbf{B} = B_0 \hat{e}_z \), the critical surface density for lateral contraction and fragmentation of the layer is

\[
\Sigma_{\text{crit}} \sim \left[ \frac{5}{G} \frac{B_0^2}{3\pi} \right]^{1/2} \sim 44 \, M_\odot \, \text{pc}^{-2} \left[ \frac{B_0}{10 \, \mu \text{G}} \right]
\]  

(Mestel 1965, his equation 85). Thus, the magnetic field will only have a significant influence on the dynamics of the undisturbed layer if \( \Sigma_{\text{layer}} \lesssim \Sigma_{\text{crit}} \), i.e. if

\[
B_0 \gtrsim 32 \, \mu \text{G} \, Z_{10}^{-1} \, n_4.
\]

### 8.7.2 Magnetic resistance to the advance of the IF

The ram pressure of the ionized gas flowing off the IF is

\[
P_{\text{ram}}(r) = \frac{n_{\text{ws}}(r) v_{\text{ws}}^2}{2}
\]

\(~1.4 \times 10^{-9} \, \text{erg cm}^{-3} \, Z_{10}^{-1/3} \, n_4^{1/3} \, N_{10}^{-1/3} \, [\text{t/Myr}]^{-2/3}.\)

The magnetic pressure is

\[
P_{\text{mag}} = \frac{B_0^2}{8\pi} \sim 4 \times 10^{-12} \, \text{erg cm}^{-3} \left[ \frac{B_0}{10 \, \mu \text{G}} \right]^2.
\]

Therefore, expansion of the newly ionized gas in the immediate vicinity of the IF is not significantly slowed by the magnetic field. Moreover, as the gas flows further away from the IF its ram pressure only decreases quite slowly (approximately as \( r^{-1} \)). Since the ionization balance is dominated by recombinations in the immediate vicinity of the IF, the magnetic field should have little effect on the advance of the IF. In the HiiR, the magnetic field will simply be advected by the ionized gas.

### 8.8 Star formation in the SUR

It is certainly possible that a second generation of stars will form in the SUR. However, without knowing details of the turbulence there (i.e. how much is in wavelengths that can be rendered unstable against collapse), it is impossible to evaluate this possibility. Such considerations lie outside the scope of the current paper, and would almost certainly have to be addressed with numerical simulations, and a slew of additional parameters regulating the initial and boundary conditions, and the constitutive physics.

### 9 DISCUSSION

We have explored the possibility that, if an O star, or compact group of OB stars, forms in a shock-compressed layer and stays close to the mid-plane of the layer, then it will carve out an approximately circular hole in the layer. Ionized gas will steam away above and below the layer, producing a bipolar HiiR. At the waist of the bipolar HiiR, an IF will be driven into the layer, producing an approximately circular bright rim, and sweeping up a ring of dense shocked gas, within which a second generation of stars may form.

#### 9.1 Observed morphology

The observed morphology of such a configuration will depend strongly on the viewing angle, relative to the normal to the layer (here the z-axis) and on the wavelength, due to dust extinction.

Observers who are close to the z-axis, and therefore view the layer close to face-on, will see an approximately circular bright rim, which might in the first instance be interpreted with a limb-brightened spherically symmetric model – except that the column densities of ionized and neutral gases through the middle of the ring will be significantly lower than expected. Hence, the model might offer a straightforward explanation for the cylindrical HiiRs observed by Beaumont & Williams (2010).

Observers close to the \( z = 0 \) plane will see a bipolar HiiR. Any difference between the size and brightness of the lobes would be attributable to the source (or sources) of ionizing radiation having moved away from the mid-plane of the layer, although the HiiR would cease to be bipolar if this movement were too great. Further asymmetry might also derive from differential extinction due to the dust in the layer.

It follows that there will probably be a range of intermediate angles relative to the z-axis, from which the projected morphology of the HiiR – even if it is intrinsically bipolar, and conforms to our model – will be quite complicated and hard to interpret.

#### 9.2 Overall dynamics and mass budget

The IF advances quite rapidly into the layer, typically at speeds exceeding 1 km s\(^{-1}\), sweeping up mass into a dense ring where a second generation of stars may form. Ionized gas flows off the IF and escapes above and below the layer at an approximately constant rate, but most of the mass that is shifted to create the hole in the layer ends up in the dense ring between the IF and the SF.

#### 9.3 Comparison with feedback in a filament

The expressions derived here for the rate at which the IF advances (equation 47), the mass of ionized gas (equation 52), and the mass of gas in the SUR (equation 59) can be compared with those obtained in Whitworth & Pringle (2001) for the case of an O star formed in, or at the end of, a filament.

The rate of advance of the IF has approximately the same dependence on the half-thickness of the undisturbed layer (\( \text{vice} \) the radius of the undisturbed filament), the density in the undisturbed layer (\( \text{vice} \) the density in the undisturbed filament), the ionizing output of the O star, and the elapsed time since switch-on. This is because the conditions at the IF are largely dictated by the ionizing output, \( N_{\text{ion}} \), and by physical conditions ahead of the IF (i.e. the density and sound speed in the undisturbed layer (\( \text{vice} \) filament).

However, the mass of ionized gas flowing off the IF and the mass of neutral gas swept up between the IF and the SF both have different dependences, due to the different geometries. For the layer considered here, the mass of ionized gas increases linearly with time, whereas for the filament the mass of ionized gas only increases as \( t^{1/3} \). Similarly, for the layer, the mass of swept-up neutral gas increases as \( r^{1/4} \), whereas for the filament it only increases as \( r^{2/3} \). This is basically because, as the IF moves further away from the O star, the solid angle...
presented by the (edge-on) layer decreases much more slowly than the solid angle presented by the (end-on) filament.

We note that the advance of the IF into the layer does not stall, and nor does the advance of the IF into the filament in Whitworth & Priestley (2021). If the O star were to emit ionizing radiation for ever, and the layer were of infinite two-dimensional extent, or the filament were of infinite length, the IF would continue to advance indefinitely, albeit at an ever-decreasing rate. This is because, in these two situations, the ionized gas boiling off the IF diverges and escapes, in principle to infinity; it does not stick around for long on the path taken by ionizing photons from the O star to the IF, and therefore its re-ionization (following recombination) does not use up many of these photons. The advance of the IF slows down because the flux of ionizing radiation reaching the IF decreases due to geometric dilution. This contrasts with the situation where an O star is placed in a uniform medium and ionizes a spherical HiiR. In that case, the resulting HiiR expands until there is pressure balance between the relatively diffuse but hot gas of the HiiR and the relatively dense but cold gas of the surrounding neutral medium, and the advance of the IF then stalls (e.g. Bisbas et al. 2015); thereafter, all the ionizing output of the O star is expended balancing recombination in a static, spherical HiiR.

10 CONCLUSIONS

We have developed a simple model for the feedback from an O star (or equivalently a compact cluster of OB stars), formed in a dense layer such as might result from the collision of two clouds or two colliding streams.

Similarly to the model developed in Whitworth & Priestley (2021) for feedback from an O star formed in, or at the end of, a filament, the model developed here is based on a number of simplifying assumptions, in particular (i) that the O star remains close to the mid-plane of the layer, (ii) that the resulting HiiR is approximately circular when projected on to the mid-plane of the layer, and (iii) that the radius of curvature of the IF, where it eats into the layer, is approximately equal to the half-thickness of the layer.

We derive power-law expressions for the key parameters, in terms of $Z_{\text{out}} = Z_{\text{layer}} / 0.1 \text{pc}$ (where $Z_{\text{layer}}$ is the half-thickness of the undisturbed layer), $n_4 = n_{\text{layer}} / 10^4 \text{cm}^{-3}$ (where $n_{\text{layer}}$ is the volume density of molecular hydrogen in the undisturbed layer), and $Z_{\text{out}} = N_{\text{out}} / 10^{20} \text{s}^{-1}$ (where $N_{\text{out}}$ is the rate at which the O star emits ionizing photons).

The distance from the O star to the IF, $W_{\text{IF}}(t)$, and the speed of advance of the IF are given by

$$W_{\text{IF}}(t) = 3.8 \text{ pc } Z_{\text{out}}^{1/6} n_4^{1/3} N_{\text{out}}^{1/6} \text{ [Myr]^{2/3}},$$

$$dW_{\text{IF}}/dt = 2.3 \text{ km s}^{-1} Z_{\text{out}}^{1/6} n_4^{1/3} N_{\text{out}}^{1/6} \text{ [Myr]^{-1/3}},$$

(see Section 5).

The rate at which ionized gas is boiled off the IF is given by

$$dM_{\text{IF}}/dt \approx 350 M_\odot \text{ Myr}^{-1} Z_{\text{out}}^{1/2} N_{\text{out}}^{1/2},$$

and is constant. The total mass of ionized gas is

$$M_{\text{IF}}(t) \approx 350 M_\odot Z_{\text{out}}^{1/2} N_{\text{out}}^{1/2} \text{ [Myr]}$$

(see Section 6).

The rate at which the gas in the layer is swept up and compressed into a ring immediately ahead of the IF is

$$dM_{\text{SUR}}/dt \approx 8500 M_\odot \text{ Myr}^{-1} Z_{\text{out}}^{2/3} n_4^{1/3} N_{\text{out}}^{1/3} \text{ [Myr]^{4/3}},$$

and the mass of the ring is

$$M_{\text{SUR}}(t) \approx 6400 M_\odot Z_{\text{out}}^{2/3} n_4^{1/3} N_{\text{out}}^{1/3} \text{ [Myr]^{4/3}}$$

(see Section 7).

The simplifying assumptions made in order to derive these expressions are primarily contained in the anstz (see Section 2). The key approximations made to justify the subsequent analysis, and hence the derivation of the above approximate expressions, are justified retrospectively in Section 8.

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DATA AVAILABILITY

All software used will be supplied on request to APW.

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