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Covid-19 classification by FGCNet with deep feature fusion from graph convolutional network and convolutional neural network

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ABSTRACT

(Aim) COVID-19 is an infectious disease spreading to the world this year. In this study, we plan to develop an artificial intelligence based tool to diagnose on chest CT images.

(Method) On one hand, we extract features from a self-created convolutional neural network (CNN) to learn individual image-level representations. The proposed CNN employed several new techniques such as rank-based average pooling and multiple-way data augmentation. On the other hand, relation-aware representations were learnt from graph convolutional network (GCN). Deep feature fusion (DFF) was developed in this work to fuse individual image-level features and relation-aware features from both GCN and CNN, respectively. The best model was named as FGCNet.

(Results) The experiment first chose the best model from eight proposed network models, and then compared it with 15 state-of-the-art approaches.

(Conclusion) The proposed FGCNet model is effective and gives better performance than all 15 state-of-the-art methods. Thus, our proposed FGCNet model can assist radiologists to rapidly detect COVID-19 from chest CT images.

1. Introduction

COVID-19 (also known as coronavirus) was declared as a Public Health Emergency of International Concern on 30/01/2020, and declared as a worldwide pandemic on 11/03/2020 [1]. Till 16/Sept, this COVID-19 pandemic caused 29.6 million confirmed cases and 936.9 thousand death tolls (US 199.1k deaths, Brazil 133.2k deaths, India 82.0k deaths, Mexico 71.6k deaths, UK 41.6k deaths, etc.)

Two prevalent diagnosis are available. One is viral testing via a nasopharyngeal swab to test the presence of viral RNA fragments. The samples are then tested by the method of real-time reverse transcription polymerase chain reaction (rRT-PCR) [2]. In some situation, a nasal swab or sputum sample may also be used. Results of rRT-PCR are generally available within some hours to two days. Another is imaging methods, among which the chest computed tomography (CCT) is one of the imaging devices that can provide the highest sensitivity. The main biomarkers in CCT differentiating COVID-19 from healthy people are the asymmetric peripheral ground-glass opacities (GGOs) without pleural effusions. The advantages of imaging methods are that they could aid in screening or accelerate the speed of diagnosis, especially with shortages of RT-PCR [3].

However, manual interpretation by radiologists is tedious and easy to be influenced by inter-expert and intra-expert factors (such as fatigue, emotion, etc.). Besides, the diagnosis throughput by human experts are...
not comparable with machines. Particularly, early symptoms are smaller, which may be neglected by human experts. Smart diagnosis systems via computer vision and artificial intelligence can benefit patients, radiologists, experts and hospitals.

Traditional artificial intelligence (AI) and modern deep learning (DL) methods have achieved excellent results in analyzing medical images, e.g., Lu [4] proposed a radial-basis-function neural network (RBFNN) to detect pathological brains. Yang [5] presented a kernel-based extreme learning classifier (KELM) to create a novel pathological brain detection system. Their methods were robust and effective. Lu [6] proposed a novel extreme learning machine trained by the bat algorithm (ELM-BA) approach. Li and Liu [7] employed a real-coded biogeography-based optimization (RCCBO) for pathological brain detection, and this RCCBO method can be transferred to COVID-19 detection. Jiang [8] proposed a six-layer convolutional neural network with leaky rectified linear unit for fingerspelling recognition. Their method was shorted as 6L-CLF. Szegedy, et al. [9] presented the GoogleNet. Guo and Du [10] suggested the use of ResNet-18 for thyroid ultrasound classification. Fulton, et al. [11] employed ResNet-50 for classification of Alzheimer’s disease. Their method is called RN-50-AD. Togacar, et al. [12] used SqueezeNet and MobileNetV2 to extract features, and employed social mimic optimization (SMO) for feature selection and combination. Cohen, et al. [13] used a large non-COVID-19 chest X-ray set to construct features for COVID-19 images. They authors predicted geographic extent score and lung opacity score to gauge severity of COVID-19 infection. Their method was abbreviated as Covid severity score net (CSSNet) in short. Loey, et al. [14] used generative adversarial network (GAN) to generate more images, and they found GoogleNet with GAN works better for two-class classification. They method was called GGNet. Li, et al. [15] used ResNet50 as the backbone. The CNN features were combined by a max-pooling operation. The resulting feature map was fed to a fully-connected layer to generate the probability score of COVID-19, community acquired pneumonia (CAP), and non-pneumonia. Their method was called COVNet. Ni, et al. [16] used 3D U-Net and MVP-Net on 96 COVID-19 patients in CCT images, for pulmonary lobe segmentation, COVID-19 lesion detection and COVID-19 lesion segmentation. Their method is called NiNet in this study. Ko, et al. [17] proposed a simple 2D deep learning framework for single CCT image. The authors compared four pre-trained models: VGG16, ResNet-50, Inception-V3, and Xception. They found ResNet-50 showed the best performance. The authors used two augmentation method: image rotation and zoom. Their proposed additional layers consist of a flatten layer, a fully connected layer with 32 neurons, and a fully connected layer with 3 neurons. Their model can classify three classes: non-pneumonia, other pneumonia, and COVID-19. Their method was named as fast-track COVID-19 classification network (FCONet). Wang, et al. [18] developed a weakly-supervised deep learning framework using 3D CT volumes for COVID-19 classification and lesion localization. In their method, the lung region was segmented via a pre-trained UNet. The segmented 3D lung region was fed into a 3D deep neural network to predict the COVID-19 infection probability. Their method was named 3D deep convolutional neural network to detect COVID-19 (DeCovNet). Tabik, et al. [19] proposed a COVID-SDNet for predicting COVID-19 based on chest X-ray images.

However, most of the existing COVID-19 algorithms above employed single feature representation (SFR), and ignore fusing multiple feature representations (MFRs). Commonly, MFRs can yield better results than using any SFR, because MFR is more informative and accurate than any SFR, and MFR consists of all the necessary information. The disadvantages of MFR are (i) they are of high-dimensionality and needs fusion technology, but fuse sometimes will introduce the distortion into the fused features; (ii) Fusion is not a static process in nature; (iii) Fusion of trivial features may affect the results. For example, Hasan, et al. [20] fused MFRs in robust hemolytic peptide prediction. Their cross-validation results showed their method outperformed state-of-the-art approaches. Li, et al. [21] used kernel sparse MFRs for hyperspectral (HS) image classification. Their method gave better results than state-of-the-art HS image classification methods. There are more success cases of using MFRs yielding better performances than SFR.

The main contribution of this paper is deep feature fusion (DFF), viz., the fuse of multiple deep feature representations from both convolutional neural network (CNN) and graph convolutional network (GCN). CNN yields individual image-level representation (IIR), while GCN yields relation-aware representation (RAR). Hence, IIR and RAR are fused together at feature-level, and experiments proved the DFF proposed is efficient, and the fused features give better performances than using IIR features alone. Particularly, our method addresses related subproblems, e.g., feature selection, feature fusion, classifier selection. The resulting system is an efficient pipeline for COVID-19 diagnosis. We propose a fully automatic method which aims to ease the burden of the radiologist. Other contributions of this study are: (i) we propose to use batch normalization and dropout to our deep neural network model; (ii) we use rank-based average pooling to replace traditional max pooling; (iii) we propose multiple-way data augmentation. Finally, our model was demonstrated to give better performance than state-of-the-art approaches.

### 2. Dataset and preprocessing

Tables 12 and 13 itemized the abbreviation and mathematical symbols used in this study for easy reading. See Appendix A and Appendix B.

#### 2.1. Dataset

Image acquisition CT configuration and method: Philips Ingenity 64 row spiral CT machine, KV: 120, MAS: 240, layer thickness 3 mm, layer spacing 3 mm, screw pitch 1.5: lung window (W: 1500 HU, L: –500 HU), Mediastinum window (W: 350 HU, L: 60 HU), thin layer reconstruction according to the lesion display, layer thickness and layer distance are 1 mm lung window image. The patients were placed in a supine position, breathing deeply after holding in, and conventionally scanned from the lung tip to the costal diaphragm angle.

For each subject, 1–4 slices were chosen by radiologists using slice level selection method, because usually 4 slices are sufficient to cover the lesion. For COVID-19 pneumonia patients, the slice showing the largest size and number of lesions was selected. For normal subjects, any level of the image can be selected.

The resolutions of all selected images are 1, 024 × 1, 024 × 3. Table 1 lists the demographics of subjects, where we have two categories: (i) COVID-19 patient, and (ii) healthy control (HC) subjects.

| Subject nos | Image nos. | Age range |
|-------------|------------|-----------|
| COVID-19    | 142        | 320       | 22–91 |
| HC          | 142        | 320       | 21–76 |

When there are differences between the analyses of two junior radiologists (A1, A2), a superior doctor (A3) was consulted to reach a consensus. Suppose X means a CCT scan, L means the labeling of each individual expert, and the final labeling Lis obtained by

\[
\hat{L}(X) = \begin{cases} 
L(A_1) & \text{if } MV(L_{all}) \\
L(A_2) & \text{otherwise}
\end{cases}
\]  \tag{1}

where \(L_{all}\) represents the labeling of all experts, i.e., \(L_{all} = [L(A_1), L(A_2), L(A_3)]\) \(MV\) denotes majority voting.

#### 2.2. Preprocessing

The original dataset containing 320 COVID-19 images and 320 HC
get the resized image set $U_5$ as

$$U_5 = \{ u_1(i), u_2(i), ..., u_s(i), ... u_s([U]) \}$$

where $\psi: x \rightarrow y$ means the downsampling (DS) function, where $y$ is a downscaled image of original image $x$. In this study, $W_5 = H_5 = 256$, $C_5 = 1$. The advantage of DS are two parts: (i) It can save storage, as shown in Table 2, (ii) Smaller-size dataset can help the following classification system from overfitting. The reason why we set $W_5 = H_5 = 256$is based on trial-and-error method. We found that larger size will bring in overfitting which impairs the performance, and meanwhile, smaller size will make the images blurry which also decreases the classifier’s performances.

Table 2 compares the size and storage of each image $u_s(i), s = 1, \ldots, 5$, $i = 1, \ldots, [U]$ at every preprocessing step. We can see here after preprocessing procedure, each image will only cost about 2.08% of its original storage or size. The compression ratio (CR) rates of ith image of final stage $U_5$ to original stage $U_1$ were calculated as. CR$_{\text{storage}}(i) = \text{byte}[u_s(i)]/\text{byte}[u_1(i)] = 262, 144/12, 582, 912$, and CR$_{\text{size}}(i) = \text{size}[u_s(i)]/\text{size}[u_1(i)] = 65.536/3, 145, 728$. Hence, we can get CR$_{\text{size}}(i) = \text{CR}_{\text{size}}(i) = 2.083\%$, $\forall i = 1, 2, ..., [U]$. Fig. 2(a and b) shows two samples (COVID of a and HC of b) from the preprocessed dataset $U_5$. Fig. 2(c) delineates the lesions of (a) within red circles.

3. Methodology

The motivation of this study is two-fold. First, we plan to create a customary state-of-the-art comparable convolutional neural network with several improvements, including batch normalization, dropout, rank-based average pooling, and multiple-way data augmentation. This motivation of using CNN is to extract individual image-level representation (IRR). Nevertheless, CNN cancels out the relation of a particular image among a group of images. In contrast, this relation-aware representation (RAR) can be captured by graph convolutional network (GCN). Hence, the second main motivation is (i) to use GCN to establish connectivity analysis and extract RAR features; and (ii) to fuse CNN features and GCN features together to enhance the classifier’s performance.

Using GCN with CNN can obtain better performance than using CNN merely. Shi, et al. [22] used GCN for cervical cell classification. Their results were significantly better than ResNet-101 and DenseNet-121. Bin, et al. [23] used GCN to extract structure-aware human pose estimation. Their experiments on single- and multi-person estimation benchmark datasets showed that GCN consistently outperforms competing state-of-the-art methods. Tian, et al. [24] proposed a novel GCN-based interactive prostate segmentation in MR images. Their method yielded mean Dice similarity coefficients of 93.8 ± 1.2% and 94.4 ± 1.0% on their in-house and PROMISE12 datasets, respectively. All those three literatures show the powerfulness of GCN.

### 3.1. Basics of CNN

Traditional machine learning achieved excellent results on disease detections [25,26]. Convolutional neural network (CNN) is a new artificial neural network. Generally, CNN is composed of conv layers (CLs),

![Illustration of preprocessing.](image-url)

**Table 2** Image size and storage per image at each preprocessing step.

| Preprocess | Symbol | $W$ | $H$ | $C$ | Size (per image) | Storage (per image) |
|------------|--------|-----|-----|-----|------------------|---------------------|
| Original   | $u_1(i)$ | 1024 | 1024 | 3   | 3,145,728        | 12,582,912          |
| Grayscale  | $u_2(i)$ | 1024 | 1024 | 1   | 1,048,576        | 419,430             |
| HS         | $u_3(i)$ | 1024 | 1024 | 1   | 1,048,576        | 419,430             |
| Crop       | $u_4(i)$ | 724  | 724  | 1   | 524,176          | 2096,704            |
| DS         | $u_5(i)$ | 256  | 256  | 1   | 65,526           | 202,144             |

...
pooling layers (PLs), non-linear activation functions (NLAFs) and fully connected layers (FCLs) [27,28].

The essential operation in CNN is convolution. A complete CL performs 2D convolution along the width and height directions [29]. Note that the weights in CNN are initialized randomly, and then weights are learnt from the data itself by network training. Fig. 3 illustrates the pipeline of input feature maps passing across a complete CL.

Fig. 3 shows there are three steps during a complete conv layer: (i) Kernel-based convolution; (ii) Stack; (iii) NLAF. Assume there is an input matrix $\Gamma$, kernels $Q_j$, $\forall j \in [1, \ldots, J]$, and an output $T$, (here output $T$ means output of the whole three-step complete conv layer, not the output of merely convolution operation). Note a conv layer means the layer runs convolution, and the “complete conv layer” means the combination of the conv layer; the stack, and NLAF. In Fig. 3, we used the same color to denote the input and output, because the output is the input of next conv layer.

For each kernel $Q_j$, the convolution output is

$$ f(j) = \Gamma \otimes Q_j, \forall j \in [1, \ldots, J] $$

where $\otimes$ means convolution operation. Then, all $f(j)$ matrixes are stacked into a three-dimensional matrix $F$.

Step2: $F = [f(1), \ldots, f(J)]$

where means the stack operation. Finally, the matrix $F$ is passed into the NLAF and output the final matrix [30]

$$ T = \text{NLAF}(F) $$

We can calculate their sizes $S$ of three main components (input, kernel, and output) as

$$ S(x) = \begin{cases} 
W_\Gamma \times H_\Gamma \times C_\Gamma & x = \Gamma \\
W_Q \times H_Q \times C_Q & x = Q_j, \forall j \in [1, \ldots, J] \\
W_T \times H_T \times C_T & x = T 
\end{cases} $$

Where the triple elements $(W, H, C)$ represent the size of height, width, and channels of the matrix, respectively [31]. The subscript $\Gamma$, $Q$, and $T$ represent input, kernel, and output, respectively. $J$ denotes total number of filters. Note that $C_T = C_Q$, which means the channel of input $C_\Gamma$ should equal the channel of kernel $C_Q$.

Assume those filters move with padding of $v_p$ and stride of $v_s$, we can get the sizes $(W_T \times H_T \times C_T)$ of output matrix $T$ by simple math as [32]:

Fig. 2. Two samples of preprocessed dataset $U_5$.  

Fig. 3. Illustration of a complete conv layer.
\[
\begin{align*}
W_T &= 1 + \frac{(2 \times v_p + W_r - W_G)}{v_r} \\
H_T &= 1 + \frac{(2 \times v_p + H_r - H_G)}{v_r} \\
C_T &= J \quad (11)
\end{align*}
\]

where \(\lfloor \cdot \rfloor\) represents the floor function. The channel of output \(C_T\) should equal the number of filters \(J\).

For the last step, viz., the NLAF \(\beta\), it usually selects the rectified linear unit (ReLU) function [33]. Suppose \(f_{ij}\) is the entry of the matrix \(F\), we have

\[
\beta_{\text{ReLU}}(f_{ij}) = \max(0, f_{ij}) \quad (12)
\]

ReLU is preferred to traditional NLAFs such as sigmoid (SM) function and hyperbolic tangent (HT) as below:

\[
\begin{align*}
\beta_{\text{SM}}(f_{ij}) &= (1 + e^{-f_{ij}})^{-1} \\
\beta_{\text{HT}}(f_{ij}) &= \tanh(f_{ij}) \\
&= \frac{e^f - e^{-f}}{e^f + e^{-f}} \quad (13) \quad (14)
\end{align*}
\]

3.2. Improvement 1: batch normalization and dropout

The motivation of batch normalization (BAN) is to solve the “internal covariant shift (ICS)”, which means the effect of randomness of the distribution of inputs to internal CNN layers during training. The existence of ICS will worsen the CNN’s performance [34,35].

This study introduced BAN to normalize those internal layer’s inputs \(\gamma_i\) over every mini-batch (suppose its size is \(|\Gamma|\)), in order to guarantee the batch normalized output \(T = \{t_i\}\) have a uniform distribution. Mathematically, BAN is to learn a function from

\[
\{\gamma_i, i = 1, 2, \ldots, |\Gamma|\} \mapsto \{t_i, i = 1, 2, \ldots, |\Gamma|\} \quad (15)
\]

During training, the empirical mean \(\mu_e\) and empirical variance \(\phi_e\) can be calculated as

\[
\begin{align*}
\mu_e &= \frac{1}{|\Gamma|} \sum_{i=1}^{\text{|\Gamma|}} \gamma_i \\
\phi_e &= \frac{1}{|\Gamma|} \sum_{i=1}^{\text{|\Gamma|}} (\gamma_i - \mu_e)^2 \quad (16)
\end{align*}
\]

The input \(\gamma_i\) was first normalized to \(\gamma_i'\)

\[
\gamma_i' = \frac{\gamma_i - \mu_e}{\sqrt{\phi_e + \alpha_s}} \quad (17)
\]

where \(\alpha_s\) in denominator in Eq. (17) is stability factor, used to enhance the numerical stability. Now the \(\gamma_i\) have zero-mean and unit-variance characteristics. In order to have a more expressive deep neural network [36] (here expressive means the network’s expressive power, i.e., the ability to express functions), a transformation is usually carried out as

\[
t_i = A_1 \times \gamma_i' + A_2, \quad i = 1, 2, \ldots, |\Gamma| \quad (18)
\]

where the parameters \(A_1\) and \(A_2\) are two learnable parameters during training. The transformed output \(t_i \in T\) is then passed to the next layer and the normalized \(\gamma_i'\) remains internal to the current layer.

In the inference stage, we no longer have minibatch. So instead of...
calculating \( \mu_c \) and \( \phi_c \), we will calculate population mean \( \mu_p \) and population variance \( \phi_p \), and we have the output \( z_i \) at the inference stage as

\[
\hat{z}_i = A_1 \times \frac{y_i - \mu_p}{\sqrt{\phi_p + \Delta}} + A_2
\]

On the other hand, a dropout layer will be introduced before the fully-connected layer. It is a regularization technique which means randomly dropping out neurons during the training. Dropout can help avoid overfitting of deep neural networks. Srivastava, et al. [37] proposed the concept of dropout neurons (DN) by randomly drop neurons and set to zero their neighboring weights from the CNN during training. Posed the concept of dropout neurons (DN) by randomly dropping out neurons during the training. Dropout can help avoid overfitting of deep neural networks. Ragavendran [41] compared rank-based pooling with traditional pooling methods. Among rank-based pooling approaches, their advantages compared to ordinary pooling methods are:

- Ranking list is invariant under slight changes of activation values;
- Important activation values can be easily distinguished by their cognate proximal values.

Important activation values can be easily distinguished by their cognate proximal values.

3.3. Improvement 2: rank-based average pooling

The pooling function fundamentally replaces the output of a layer (particularly conv layers) with a summary statistic of the adjacent outputs at a particular position. The pooling method is capable of making less-sensitive activations in the pooled map than the original feature map to the accurate spots of structures within the image.

For a region to be pooled \( \Psi \) with size of \( n \times n \), here \( n \) means pooling size. Suppose the pixels within the region \( \Psi = \{\psi_{ij}\}, (1 \leq i, j \leq n) \) are

\[
\Psi = \begin{bmatrix}
\psi_{1,1} & \cdots & \psi_{1,n} \\
\vdots & \ddots & \vdots \\
\psi_{n,1} & \cdots & \psi_{n,n}
\end{bmatrix}
\]

![Fig. 5. A simplistic example of four pooling methods (L2P, AP, MP, and RAP).](image)

The \( l_2 \) norm pooling (L2P) calculates the \( l_2 \) norm of the given region \( \Psi \). Assume the output pooling matrix is \( P \), the L2P output \( P^{L2P}(\Psi) \) is defined as \( P^{L2P}(\Psi) = \sqrt{\sum_j |\psi_{i,j}|^2} \). In this study, we add a constant \( 1/|\Psi| \), where \( |\Psi| \) means the number of elements of region \( \Psi \). We have \( |\Psi| = n^2 \). We added the new constant \( 1/|\Psi| \) under the square root, and the constant \( 1/|\Psi| \) does not influence training and inference.

\[
P^{L2P}(\Psi) = \sqrt{\frac{\sum_j |\psi_{i,j}|^2}{|\Psi|}}
\]

The average pooling (AP) calculates the mean value in the region \( \Psi \) as

\[
P^{AP}(\Psi) = \text{average}(\Psi)
\]

The max pooling (MP) operates on the region \( \Psi \) and selects the max value.

\[
P^{MP}(\Psi) = \max(\Psi)
\]

Shi, et al. [38] proposed three different rank-based pooling approaches. Their advantages compared to ordinary pooling methods are:

- Ranking list is invariant under slight changes of activation values;
- Important activation values can be easily distinguished by their cognate proxies;
- Usage of rank can avoid scale problems arise from value-based pooling methods. Among rank-based pooling approaches, the rank-based average pooling (RAP) gives better performances than state-of-the-art tactics, and has been applied in many fields. For example, Jiang [39] added RAP to convolutional neural networks for the susceptibility-weighted imaging based cerebral microbleed detection. They got a high accuracy of 97.18%. Sun, et al. [40] added RAP between each subspace mapping layer for facial expression recognition. Their method is better than PCANet and LDANet approaches. Akhtar and Ragavendran [41] compared rank-based pooling with traditional pooling methods, and stated the advantages of rank-based pooling are they...
can assign ranks and weights to activations simultaneously.

RAP first calculate the rank matrix (RM) based on the values of each element \( \psi_i \in \Psi \), usually lower ranks \( r_i \in \{1, 2, \ldots, n^2\} \) are assigned to higher values \( \psi_i \) as

\[
\psi_i = \text{rank}\{\psi_i\} = r_i
\]

(28)

Providing tied values \( \psi_1 = \psi_2 \), a constraint is added to Eq. (28).

\[
\langle \psi_1 = \psi_2 \rangle \land \langle 1 > 2 \rangle \Rightarrow r_1 > r_2
\]

(29)

RAP output of input \( \Psi \) is \( p^{\text{RAP}}(\Psi) \), which used the \( a_{\Psi} \) greatest activations

\[
p^{\text{RAP}}(\Psi) = \frac{1}{a_{\Psi}} \sum_{\psi_i \in \Psi} (\psi_i | \psi_i \leq a_{\Psi})
\]

(30)

3.4. Improvement 3: multiple-way data augmentation

To circumvent the small-size dataset (SSD) and lack of generation (LG) problems, there are four possible types of solutions, e.g., data augmentation (DA), data generation (DG), ensemble approaches (EA), and regularization.

DA will generate fake images by perturbing existing data, such as cropping, rotation. DG create data from a sampled data source. Synthetic minority over-sampling technique (SMOTE) [42] is a typical algorithm of DG. EA methods use multiple models to obtain better predictive performance than any model alone [43]. Regularization is mainly for the weights of models. Large weights will make the models unstable, because minor variation on the inputs will yield large differences in the output for large weights. Smaller weights are regarded to be more regular (i.e., less specialized). Hence, this type of technique is called weight regularization. DA is used due to its simple and ease to realize.

We proposed a \( \eta_{\text{MDA}} \)-way multiple-way data augmentation (MDA) technology. The difference of our MDA to traditional DA is we use multiple \( \eta_{\text{MDA}} > 10 \) DA technologies. Assume the preprocessed dataset \( U_{\text{pre}} = \{u_1, \ldots, u_{\eta_{\text{MDA}}}(|U|)\} \). The dataset \( U_{\text{pre}} \) is divided into three sets:

\[
U_{\text{pre}} = \{X, X', Y\}
\]

(31)

where training set \( X' = \{x'(1), \ldots, x'(i), \ldots \} \), validation set \( X' = \{x'(1), \ldots, x'(|X'|)\} \), and test set \( Y = \{y(1), \ldots, y(|Y|)\} \). Meanwhile, the sum of sizes of training set, validation set, and test set equals to the size of preprocessed dataset, \(|X'| + |X'| + |Y| = |U_{\text{pre}}|\).

From the whole training image set \( X \), we first performed the following seven DA techniques with different MDA factors \( \eta \). Note that each MDA technique will generate \( \eta \) new images. Suppose the output MDA training set is symbolized as \( X^{\text{MDA}} \).

(i) Rotation. Rotation angle vector \( \theta \) skip the value of 0.

\[
\begin{align*}
\bar{x}^\theta(i) &= R[x'(i)] \\
&= [x^\theta_1(i, x^\theta_1), \ldots, x^\theta_n(i, x^\theta_n)]
\end{align*}
\]

(32)

where \( R \) means rotation operation.

(ii) Noise injection. The \( \chi_m^\eta \)-mean \( \chi^\eta \)-variance Gaussian noises were added to all training images to produce \( \eta_\chi \) new noised images, where \( \epsilon \) is the gray levels, and \( p \) is the probability density function. We have

\[
\begin{align*}
\bar{x}^\chi(i) &= N[x'(i)] \\
&= [x^\chi_1(i, \epsilon^\chi_1), \ldots, x^\chi_n(i, \epsilon^\chi_n)]
\end{align*}
\]

(34)

where \( N \) means the noise injection operation. We used Gaussian noise in this study because it is the most common type found in images compared to impulse noise, speckle noise, and salt and pepper noise.

(iii) Horizontal Shear (HS) transform. New \( V \) images were generated by HT transform

\[
\begin{align*}
\bar{x}^\chi(i) &= H[x'(i)] \\
&= [x^\chi_1(i, \chi^\chi_1), \ldots, x^\chi_n(i, \chi^\chi_n)]
\end{align*}
\]

(35)

where \( H \) means HS transform. HS factors \( \chi^\eta \) skip the value of \( \chi^\eta = 0 \). Mathematically, if original coordinates are \( (u, v) \), and HS transformed coordinates are \( (u_1, v_1) \), then we have

\[
\begin{align*}
\bar{x}^\chi(i) &= H(x'(i)) \\
&= [x'(i, \chi^\chi_1), \ldots, x'(i, \chi^\chi_n)]
\end{align*}
\]

(36)

Clearly, the HS transform is a special affine transform, which can be written as

\[
\begin{align*}
[u_1, v_1, 1] &= [u, v, 1] \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \end{bmatrix} \\
&= [u, v, 1] \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \end{bmatrix}
\end{align*}
\]

(37)

(iv) Vertical Shear (VS) transform.

\[
\begin{align*}
\bar{x}^\chi(i) &= V[x'(i)] \\
&= [x^\chi_1(i, \chi^\chi_1), \ldots, x^\chi_n(i, \chi^\chi_n)]
\end{align*}
\]

(38)

where \( V \) means VS transform, which ran similarly as ST transform. Particularly, the VS factor is the same as HS factor \( \chi^\eta \) and \( \eta_\chi \).

(v) Random translation (RT). All training images \( x'(i) \) were translated \( \eta_\chi \) times with random horizontal shift \( \chi^\eta \) and random vertical shift \( \eta_\chi \), both values of which are in the range of \( [-a_z, a_z] \), and obey uniform distribution.

\[
\begin{align*}
\chi^\eta_m &\sim [-a_z, a_z], \forall m \in [1, \eta_\chi] \land \forall \theta \in \{x, y\}
\end{align*}
\]

(39)

where \( a_z \) is the maximum shift factor. So, we have

\[
\begin{align*}
\bar{x}^\chi(i) &= R[T[x'(i)] \\
&= [x^\chi_1(i, \epsilon^\chi_1, \epsilon^\chi_1), \ldots, x^\chi_n(i, \epsilon^\chi_n, \epsilon^\chi_n)]
\end{align*}
\]

(40)
(vi) Gamma correction (GC). The factor of $G \chi^0$ will skip the value of 1.

$$\overline{x}^0(i) = G[x(i) | \chi^0] = [x_0^0(i, x_1^0) \ldots x_n^0(i, x_n^0)]$$ (41)

where $G$ means GC operation.

(vii) Scaling. All training images $(x'(i))$ were scaled with scaling factor $\chi^0$, skipping $\chi^0 = 1$.

$$\overline{x}(i) = S[x'(i)] = [x'_0(i), x'_1(i), \ldots x'_n(i, x_n^0)]$$ (42)

(viii) Mirror and concatenation. All the above results are mirrored, we have

$$\overline{x}^{\text{mirror}}(i) = S[\overline{x}(i)], \forall n \in \{1, 2, \ldots, \eta_{DA} \}$$ (43)

where represents the mirror function. All the $\eta_{DA}$-way results are finally concatenated as

$$\overline{x}^{\text{mirror}}(i) = \overline{x}(i) \rightarrow \overline{x}(i) \rightarrow \ldots \rightarrow \overline{x}^{\text{mirror}}(i)$$ (44)

where means concatenation, $\eta_{EF}$ the enhance factor, meaning the ratio of enhanced training set to the original training set. $\eta_{EF}$ is defined as

$$\eta_{EF} = \frac{|\chi^0(i)|}{|\chi'(i)|}$$ (45)

We can calculate $\eta_{EF} = \eta_n \times \eta_{DA} \pm 1$. Thus, the MDA can be regarded as a function, making the enhanced training set $\eta_{EF}$ times as large as raw training set $X$.

$$\{i'(i) \in X' \mapsto \{\overline{x}^{\text{mirror}}(i) \in X^{\text{mirror}} \}$$ (46)

3.5. Improvement 4: deep feature fusion by graph convolutional network

To further improve the performance, we introduced a deep feature fusion (DFF) method based on graph convolutional network (GCN). GCN helps find the relation-aware representation (RAR) [44], and thus fuse RAR from GCN with IIR from CNN.

For a given graph $G = (V, E)$, where we have $|V|$ nodes $v_i \in V, i = 1, \ldots, |V|$ and corresponding links $(v_i, v_j) \in E$. We can define an adjacency matrix $A \in |V| \times |V|$ which embeds the relationship of all nodes. The purpose of GCN is to encode the graph $G$ via a neural network model $f(X, A)$ where $X \in |V| \times D$, where $D$ means the feature dimension of each node [45]. Note that $AX$ means the sum of all neighboring features. So GCN can capture the RAR information [46].

A multi-layer GCN will update the node features based on following layer-wise rule:

$$H^{l+1} = f_{\text{ReLU}}(\hat{A}H^lW)$$ (47)

where $\hat{A} \in |V| \times |V|$ represents the normalized version of adjacency matrix $A$. $f_{\text{ReLU}}$ is ReLU function. The variable $H^l \in |V| \times d_l$ is the feature representation at $l$th layer [47].

To carry out the normalization $A \rightarrow \hat{A}$, we first calculate the degree matrix $\delta \in |V| \times |V|$, which is a diagonal matrix

$$\delta_{ij} \text{ def } \begin{cases} \deg(v_i) & \text{if } i = j \\ 0 & \text{otherwise} \end{cases}$$ (48)

The normalized $\hat{A}$ is obtained based on original adjacency matrix $A$ and degree matrix $\delta$ [48].

Note the input $X = H^0$, so for a two-layer GCN as shown in Fig. 6, we have

$$H^{(1)} = f_{\text{ReLU}}(\hat{A}XW^{(0)})$$ (49.a)

$$H^{(2)} = f_{\text{ReLU}}(\hat{A}H^{(1)}W^{(1)})$$ (49.b)

where $W^{(0)} \in d_0 \times d_1$, and $W^{(1)} \in d_1 \times d_2$ are two trainable weight matrices. $(d_0, d_1, d_2)$ are hyperparameters will be set in the experiment.

In our COVID-19 classification task, the GCN will be fused with previous CNN models $N(1) \sim N(4)$. The last FCL in previous CNN models is used as the individual image-level representation (IIR) $I \in d_l$. Afterwards, k-means clustering (KMC) is performed on those image-level representation features, and we can get $|V|$ cluster centroids $X \in |V| \times d_l$. The clustering correlation shows the potential relationships of images. The adjacency matrix $A \in |V| \times |V|$ is defined as

![Fig. 6. Illustration of a two-layer GCN. (Different color cylinders mean different cluster centroids).](image)

![Fig. 7. Illustration of KNN-based adjacency matrix.](image)
Algorithm 1
Proposed deep feature fusion.

Input: IIR Feature I from CNN models
Algorithm of DFF
Step 1: Create RAR features \( H^{(2)} \) from pre-constructed two-layer GCN model
Step 2: Dot product fusion combining IIR features and RAR features, \( y = H^{(2)}I \)
Step 3: Linear Projection, \( z = yW^{(2)} + b \)
Step 4: Softmax and cross-entropy (CE) loss

\[
A_{uv} = \begin{cases} 
1 \text{ if } X_u \in \Delta(X_v) \lor X_v \in \Delta(X_u) \\
0 \text{ otherwise}
\end{cases}
\]  

(50)

where \( \lor \) means operation “or”, \( \Delta \) means the k-nearest neighbors (kNN) based on cosine similarity. The number of neighbors in kNN is symbolized as \( \Delta \).

Fig. 7 shows an example, the three nearest neighbors of node \( i \) and node \( j \) are \( \Delta(X_i) = (1, 2, j) \), \( \Delta(X_j) = (3, 4, 5) \). So, we have \( X_j \in \Delta(X_i) \), \( X_i \notin \Delta(X_j) \). Using the ‘or’ operation we can conclude \( A_{ij} = 1 \). The node features X and adjacency matrix \( A \) are sent into two-layer GCN, and we can get \( H^{(2)} \in |V| \times d_1 \). The fusion between \( H^{(2)} \) and \( I \) is accomplished by dot product fusion. Note we need to set \( d_0 = d_2 \), \( y = H^{(2)}I \)  

(51)

A linear projection (LP) with learnable weight \( W^{(2)} \in |V| \times C \), where \( C \) means the number of categories, we have

\[ z = yW^{(2)} + b \]  

(52)

where \( z \in C \), and \( b \) represents the bias. \( C = 2 \) in this study because our task is a binary classification problem, i.e., COVID-19 and healthy people. Finally, softmax operation were performed on \( z \), and cross entropy (CE) loss were calculated. Algorithm 1 shows the proposed deep feature fusion algorithm. During inference stage, the CNN’s IIR features are gained and its corresponding GCN’s RAR features are obtained by pre-constructed graph and trained two-layer GCN. Using both CNN and GCN, each image is represented by the fusion of its individual image-level representations and its relation-aware representations [22]. Fig. 8 shows the fusion flowchart.

3.6. Summary of proposed eight networks

In total, we proposed eight new networks \( \{N(1), \ldots, N(8)\} \): (i) We first designed a base network \( N(1) \), \( N(1) \) is called the base network (BN). (ii) we added batch normalization (BAN) and dropout (DO) techniques, and obtained the improved network \( N(2) \) named as “BDBN”. (iii) Next, we developed \( N(3) \) termed BDRBN, by introducing rank-based average pooling (RAP) to replace traditional max pooling (MP) in \( N(2) \). (iv) Multiple data augmentation (MDA) was proposed and added to \( N(3) \), so we get new network \( N(4) \), which is short named as BDRMBN.

For the rest four networks, we add a new deep feature fusion (DFF) approach that combines the features from above networks \( \{N(1), N(2), N(3), N(4)\} \) to RAR features from 2-layer GCN. The short names of \( \{N(5), N(6), N(7), N(8)\} \) are defined as DBN, DBDBN, DBDRBN, DBDRMBN.

Table 3 gives all the eight proposed network relationships.

As our expectation, the best model should be within \( N(5-8) \) since they fuse the features from CNNs \( N(1-4) \) with GCN. The best model will have a formal name as FGCNet, which means Fusion of GCN and CNN networks.

The configuration of proposed networks was designed by trial-and-error method. We set the number of conv layers as \( u \). Similarly, the number of FCL layers is symbolized as \( u \). The details of the base network can be found in Table 6.

3.7. Measures

The algorithm will run \( W \) runs, which help to reduce the randomness. At each run \( w = 1, 2, \ldots, W \), the ideal \( E^* \) and real \( E \) confusion matrix over validation set are

\[
\text{Table 3}
\]

| Index | Inheritance | Short Name | Description |
|-------|-------------|------------|-------------|
| N(1)  | BN          |            | Base Network |
| N(2)  | ←(N(1)+BAN)+DO | BDBN       | Add BAN and DO to N(1) |
| N(3)  | ←(N(2)+MP)+RAP | BDRBN      | Use RAP to replace MP in N(2) |
| N(4)  | ←(N(3)+MDA) | BDBRN      | Add MDA to N(3) |
| N(5)  | ←(N(1)+DFF) | DBN        | Add DFF to N(1) |
| N(6)  | ←(N(2)+DFF) | DBDBN      | Add DFF to N(2) |
| N(7)  | ←(N(3)+DFF) | DBDRBN     | Add DFF to N(3) |
| N(8)  | ←(N(4)+DFF) | DBDRMBN    | Add DFF to N(4) |

(*) Experiment below shows N(8) gives the best performance, and we name it as FGCNet.

Fig. 8. Flowchart of deep feature fusion strategy. (LP = Linear Projection; CE = Cross Entropy).

S.-H. Wang et al.  Information Fusion 67 (2021) 208–229
Algorithm 2
Pseudocode of our algorithm.

| Phase I: Preprocessing $U_1 \to U_5$ |
|-------------------------------------|
| Grayscaling: $U_1 \to U_2$. See Eq. (2). |
| HS: $U_2 \to U_3$, See Eq. (4). |
| Crop: $U_3 \to U_4$. See Eq. (5). |
| Downsampling: $U_4 \to U_5$. See Eq. (6). |

| Phase II: Model Initialization |
|--------------------------------|
| $N(1)$: Create a base network. See Figure 9(a). |
| $N(2)$: See Figure 9(b). |
| Add BAN to conv layers of $N(1)$. See Eqs. (18)(19). |
| Add DO to fully connected layers of $N(1)$. See Eqs. (21)(22). |
| $N(3)$: Replace MP with RAP. See Eq. (30) and Figure 9(c). |

| Phase III: Model Validation |
|-----------------------------|
| Split preprocessed dataset $U_5$ into test set $Y$ and non-test set $U_5 \setminus Y$. |

for $w = 1:W$ % $w$ is run index

Step III.A Random Split
Randomly split non-test set into training set $X^t(w)$, validation set $X^v(w)$.

Step III.B MDA on training set
for $i = 1:|X^t(w)|$

| Training image: $x^t(i, w)$ and its ground truth labels $\hat{L}[x^t(i, w)]$. |
| $x^t(i, w)$: $i$-th training image in $w$-th run |
| $x^t(i, w) \to x^{ID}(i, w)$. See Eq. (46). |
end

Enhanced training set: $X^{ID}(w) = \{x^{ID}(i, w) | i = 1, \ldots, |X^t(w)|\}$.
Enhanced training set labels: $\hat{L}(w) = \{\hat{L}[x^t(i, w)] | i = 1, \ldots, |X^t(w)|\}$.

Step III.C Training on eight proposed models
for $n = 1:8$ % $n$ is the model index

| Create an initial model $N(n, w)$; |
| Train $N(n, w)$ with training set |
| Record the trained model $N(n, w)$ |
if $n == 4 \lor n == 8$

| $N(n, w) = \text{trainnetwork}\{N(n), X^{ID}(w), \hat{L}(w)\}$. |
else

| $N(n, w) = \text{trainnetwork}\{N(n), X^t(w), \hat{L}(w)\}$. |
end
end
\[ E_i(w) = \begin{bmatrix} |X|^2 & 0 \\ 0 & |X|^2 \end{bmatrix}, \quad \forall w \in 1, \ldots, W \] (53)

where \(|X|^2\) is because we have a balanced dataset. If the confusion matrix was run on the test set, then the diagonal elements turn to \(\frac{|X|^2}{3}\). In a realistic situation, suppose we have a confusion matrix as

\[ E_r(w) = \begin{bmatrix} a_1(w) \\ a_2(w) \\ a_3(w) \\ a_4(w) \end{bmatrix}, \quad \forall w \in 1, \ldots, W \] (54)

where the four variables \((a_1(w), a_2(w), a_3(w), a_4(w))\) represent TP, FN, FP, and TN at \(w\)-th run, respectively. Here P means COVID-19 and N means healthy lung. TP means a COVID-19 image is classified correctly as COVID-19, FN means a COVID-19 image is wrongly classified as healthy, FP means a healthy lung is wrongly classified as COVID-19, and TN means a healthy lung is classified correctly as healthy. It is obvious that \(0 \leq a_k(w) \leq \frac{|X|^2}{3}, \quad \forall w \in 1, \ldots, W \wedge k \in \{1, 2, 3, 4\}\) if confusion matrix

Algorithm 2 (continued)

Step III.D Validation confusion matrix

Validation Set: \(X^v(w)\) and its labels \(\hat{Y}(w)\).
Validation prediction \(\text{Pred}(n, w)\)
\(\text{Pred}(n, w) = \text{predict}[N(n, w), X^v(w)];\)
Validation performance \(E^r(n, w)\)
\(E^r(n, w) = \text{compare}[\text{pred}(n, w), \hat{Y}(w)].\) See Eq. (54).

Step III.E Indicator Evaluation

for \(m = 1: 7\) \% \(m\) is the indicator index
Extract \(\{a_1(n, w), a_2(n, w), a_3(n, w), a_4(n, w)\}\) from confusion matrix \(E^r(n, w).\)
Calculate indicators \(v^m(n, w).\) See Eq. (55)-(62).
end

Phase IV: Compare and select the best model FGCNet on Validation Set

for \(n = 1: 8\)
Calculate MSD of \(N(n)\). See Eqs. (63)(64).
end

Select the best model \(n^*\) in terms of mean accuracy
\(n^* = \arg\max\{M[v^4(n)]\}.\)
FGCNet = \(N(n^*).\)

Phase V: Report the test performance of the best model

Training set is \(U_5 - Y\), and the ground truth is \(\hat{Y}(T)\).
Test set is \(Y\), and the ground truth is \(\hat{Y}\).
for \(w = 1: W\) \% \(w\) is run index
We initialized a random seed \(S(w)\) at each run.
if \(n^* = 4 \lor n^* = 8\)
\(N(n^*, w) = \text{trainnetwork}[N(n^*), MDA[U_5 - Y], \hat{Y}(T), S(w)].\)
else
\(N(n^*, w) = \text{trainnetwork}[N(n^*), U_5 - Y, \hat{Y}(T), S(w)].\)
end
\(\text{Pred}(n^*, w) = \text{predict}[N(n^*, w), Y];\)
\(E^r(n^*, w) = \text{compare}[\text{pred}(n^*, w), \hat{Y}].\)
End
Calculate MSD of \(N(n^*)\) based on \(W\) runs of \(E^r(n^*, w).\)

Output: The best model FGCNet \(N(n^*)\) and its test performance.
run on validation set.

Four simple measures \( \{ \nu^1(w), \nu^2(w), \nu^3(w), \nu^4(w) \} \) can be below, here \( \nu^1 \) means sensitivity, \( \nu^2 \) means specificity, \( \nu^3 \) precision, and \( \nu^4 \) accuracy.

\[
\nu^1(w) = \frac{a_1(w)}{a_1(w) + a_2(w)}
\]

\[
\nu^2(w) = \frac{a_3(w)}{a_3(w) + a_4(w)}
\]

\[
\nu^3(w) = \frac{a_1(w)}{a_1(w) + a_3(w)}
\]

\[
\nu^4(w) = \frac{a_1(w) + a_4(w)}{a_1(w) + a_2(w) + a_3(w) + a_4(w)}
\]

F1 score at \( w \)-th run is defined as \( \nu^5(w) \)

\[
\nu^5(w) = \frac{2 \times a_1(w)}{2 \times a_1(w) + a_2(w) + a_3(w)}
\]

Besides, F1 score can be expressed in the format of sensitivity and precision as \( \nu^6(w) = 2 \times \nu^1(w) \times \nu^2(w) / (\nu^1(w) + \nu^2(w)) \). The F1 score \( \nu^6 \) is the harmonic mean of the precision \( \nu^2 \) and sensitivity \( \nu^1 \). The range of F1 score is \([0, 1]\). The highest possible value 1 indicates perfect precision \( \nu^2 \) and sensitivity \( \nu^1 \), and the lowest possible value 0 means either the precision \( \nu^3 \) or the sensitivity is zero \( \nu^1 \).

\[
\nu^6 = \sqrt{\frac{1}{\nu^1 \nu^2} - \frac{1}{\nu^1} - \frac{1}{\nu^2}} = 1
\]

Matthews correlation coefficient at \( w \)-th run (MCC) \( \nu^7(w) \) is defined as

\[
\nu^7(w) = \frac{a_4(w) \times a_1(w) - a_1(w) \times a_2(w)}{\sqrt{a(w)}}
\]

where \( \varepsilon(w) \) is a temporary variable defined as \( \varepsilon(w) = [a_3(w) + a_1(w)] \times [a_1(w) + a_2(w)] \times [a_4(w) + a_3(w)] \times [a_4(w) + a_2(w)] \times [a_1(w) + a_2(w)] \).

Finally, Fowlkes–Mallows index (FMI) at \( w \)-th run \( \nu^8(w) \) can be defined as:

\[
\nu^8(w) = \sqrt{\frac{a_1(w) \times a_1(w)}{a_1(w) + a_3(w) \times a_1(w) + a_2(w)}}
\]

FMI can be expressed in the terms of sensitivity and precision as \( \nu^8(w) = \sqrt{\nu^1(w) \times \nu^2(w)} \).

After recording the seven indicators of all \( W \) runs, we can calculate the mean and standard deviation (MSD) of all \( m \)-th \( (\forall m \in [1, 7]) \) measures as

\[
M(\nu^m) = \frac{1}{W} \sum_{w=1}^{W} \nu^m(w)
\]

\[
SD(\nu^m) = \sqrt{\frac{1}{W - 1} \sum_{w=1}^{W} [\nu^m(w) - M(\nu^m)]^2}
\]

The final result over \( W \) runs were reported in the form of Mean ± SD format.

3.8. Proposed algorithm

Algorithm 2 presents the pseudocode of our algorithm, composed of one input, one output, and five phases. Phase I presents the preprocessing. Phase II presents how to construct the eight network models. Phase III shows the detailed procedures of \( W \) runs over validation set. Phase IV presents how to select the best network model based on validation performance. Phase V shows to calculate the test performance using the best network model.

4. Experiments and results

4.1. Hyperparameter setting

Table 4 shows the hyperparameter setting in this study. Most of the values are set by trial-and-error method. The stability factor is set as \( 10^{-5} \). The retention probability is set as 0.5. The pooling size is set to 2. The rank threshold is set to 2. The number of DA techniques and new images per DA are set to 14 and 30, respectively. The maximum shift factor is 25, and the mean and variance of noise injection is set to 0 and 0.01, respectively. The rotation parameter vector \( \chi^H \), horizontal shift parameter vector \( \chi^L \), Gamma correction parameter vector \( \chi^G \), scaling parameter vector \( \chi^R \) are all listed here. Enhanced factor is calculated as 421. The number of conv layers and fully connected layers are set as 7 and 2, respectively. Number of cluster centroids is set to 256. Feature dimension in GCN is set as \( d_0 = d_2 = 120 \), and \( d_1 = 60 \). The number of neighbors in KNN is set to 7. The number of runs \( W \) is 10 since it is a
Where we can see the total size of training set is the default value used in many other publications. The top row of Table 5 shows the training, MDA training, validation and test set. Where we can see the total size of training set is the default value used in many other publications.

4.2. Base network configuration

The top row of Fig. 9(a) shows the activation maps of the proposed base network N(1). Here, the size of input is $S1 = 256 \times 256 \times 1$, the output of the first conv layer (C1) is $S2 = 256 \times 256 \times 32$. Then after the first pooling (P1), the output is $S3 = 128 \times 128 \times 32$. We repeat the conv layers in total seven times, and the output is $S7 = 2 \times 2 \times 512$. S15 was flattened into one column vector $S16 = 1 \times 1 \times 2048$, and passed into two fully-connected blocks (first two blocks contain FCL and ReLU, last block contains FCL and softmax), and the outputs are $S17 = 1 \times 1 \times 120$, and $S18 = 1 \times 1 \times 2$. All the 18 matrices $S(k)$, $k \in \{1, 18\}$ correspond to the cuboids in Fig. 9(b). Note S17 will be used as IIR features. The hyperparameters of N(1) are presented in Table 6. Based on N(1), we can create the rest seven networks.

4.3. Illustration of MDA

Fig. 10 shows the MDA results. The original image is Fig. 2(a). We can observe that one image will generate 421 new images. This is why we called our algorithm multiple-way data augmentation (MDA).

4.4. Comparison among proposed networks

Table 7 gives the 10 runs of results using N(1) to N(4). N(1) is BN, N(2) is BDBN, N(3) is BDRBN, and N(4) is BDRMBN. Table 7 clearly shows that N(1) model yielded the following seven performances as: $\nu_{N(1)}^1 = 89.22 \pm 2.38$, $\nu_{N(1)}^{2} = 92.50 \pm 2.31$, $\nu_{N(1)}^{3} = 92.31 \pm 2.10$, $\nu_{N(1)}^{4} = 90.86 \pm 1.28$, $\nu_{N(1)}^{5} = 90.70 \pm 1.31$, $\nu_{N(1)}^{6} = 81.82 \pm 2.53$, $\nu_{N(1)}^{7} = 90.73 \pm 1.30$. Definition of can be found in Section 3.7.

For N(2), the performances improved as $\nu_{N(2)}^1 = 94.22 \pm 1.05$, $\nu_{N(2)}^{2} = 94.69 \pm 2.47$, $\nu_{N(2)}^{3} = 94.71 \pm 2.29$, $\nu_{N(2)}^{4} = 94.45 \pm 1.40$, $\nu_{N(2)}^{5} = 94.45 \pm 1.34$, $\nu_{N(2)}^{6} = 88.93 \pm 2.78$, $\nu_{N(2)}^{7} = 94.46 \pm 1.33$. Comparing the results of BN as N(1), we can observe the effectiveness of using batch normalization and dropout.

Furthermore, N(3) yields the performances as $\nu_{N(3)}^1 = 94.53 \pm 1.69$, $\nu_{N(3)}^{2} = 95.47 \pm 2.14$, $\nu_{N(3)}^{3} = 95.47 \pm 2.05$, $\nu_{N(3)}^{4} = 95.00 \pm 1.23$, $\nu_{N(3)}^{5} = 94.98 \pm 1.23$, $\nu_{N(3)}^{6} = 90.04 \pm 2.47$, $\nu_{N(3)}^{7} = 94.99 \pm 1.23$. Comparing the seven indicator performances between BDBN of N(2) and BDRBN of N(3)

\begin{table}[h]
\centering
\caption{Hyperparameters of N(1).}
\begin{tabular}{|c|c|c|c|}
\hline
Index & Layer & Hyperparameter & Size of activation map \\
\hline
1 & Input & & \\
2 & Conv-1 & 32 & 256 \times 256 \times 1 \\
3 & P-1 & /2 & 256 \times 256 \times 32 \\
4 & Conv-2 & 64 & 128 \times 128 \times 32 \\
5 & P-2 & /2 & 128 \times 128 \times 64 \\
6 & Conv-3 & 128 & 64 \times 64 \times 64 \\
7 & P-3 & /2 & 64 \times 64 \times 128 \\
8 & Conv-4 & 128 & 32 \times 32 \times 128 \\
9 & P-4 & /2 & 32 \times 32 \times 128 \\
10 & Conv-5 & 256 & 16 \times 16 \times 16 \\
11 & P-5 & /2 & 8 \times 8 \times 256 \\
12 & Conv-6 & 256 & 8 \times 8 \times 256 \\
13 & P-6 & /2 & 4 \times 4 \times 256 \\
14 & Conv-7 & 512 & 4 \times 4 \times 512 \\
15 & P-7 & /2 & 2 \times 2 \times 512 \\
16 & Flatten & & 1 \times 1 \times 1048 \\
17 & FCL-1 & 120 & 1 \times 1 \times 120 \\
18 & FCL-2 & 2 \times 120 & 1 \times 1 \times 2 \\
\hline
\end{tabular}
\end{table}
Fig. 10. Results of proposed MDA.
### Table 7
Comparison among N(1–4) over validation set.

|   | $N(1)$ | $\nu^1$ | $\nu^2$ | $\nu^3$ | $\nu^4$ | $\nu^5$ | $\nu^6$ | $\nu^7$ |
|---|--------|---------|---------|---------|---------|---------|---------|---------|
| 1 | 89.06  | 93.75   | 93.44   | 91.41   | 91.20   | 82.90   | 91.23   |
| 2 | 93.75  | 92.19   | 92.31   | 92.97   | 93.02   | 85.95   | 93.03   |
| 3 | 90.63  | 87.50   | 87.88   | 89.06   | 89.23   | 78.16   | 89.24   |
| 4 | 89.06  | 92.19   | 91.94   | 90.63   | 90.48   | 81.29   | 90.49   |
| 5 | 90.63  | 92.19   | 92.06   | 91.41   | 91.34   | 82.82   | 91.34   |
| 6 | 89.06  | 93.75   | 93.44   | 91.41   | 91.20   | 82.90   | 91.23   |
| 7 | 89.06  | 95.31   | 95.00   | 92.19   | 91.94   | 84.54   | 91.98   |
| 8 | 85.30  | 90.63   | 90.32   | 89.06   | 88.89   | 78.16   | 88.90   |
| 9 | 84.38  | 95.31   | 94.74   | 89.84   | 89.26   | 80.17   | 89.41   |
| 10| 87.50  | 95.31   | 94.74   | 89.84   | 89.26   | 80.17   | 89.41   |

**MSD (N(1))**: 89.22 ± 2.38

|   | $N(2)$ | $\nu^1$ | $\nu^2$ | $\nu^3$ | $\nu^4$ | $\nu^5$ | $\nu^6$ | $\nu^7$ |
|---|--------|---------|---------|---------|---------|---------|---------|---------|
| 1 | 93.75  | 95.31   | 95.24   | 94.53   | 94.49   | 89.07   | 94.49   |
| 2 | 95.31  | 96.88   | 96.83   | 96.09   | 96.06   | 92.20   | 96.07   |
| 3 | 93.75  | 95.31   | 95.24   | 94.53   | 94.49   | 89.07   | 94.49   |
| 4 | 95.31  | 93.75   | 93.85   | 94.53   | 94.57   | 89.07   | 94.58   |
| 5 | 95.31  | 96.88   | 96.83   | 96.09   | 96.06   | 92.20   | 96.07   |
| 6 | 95.31  | 95.31   | 95.31   | 95.31   | 95.31   | 90.63   | 95.31   |
| 7 | 93.75  | 92.19   | 92.31   | 92.97   | 93.02   | 85.95   | 93.03   |
| 8 | 92.19  | 96.88   | 96.72   | 94.53   | 94.40   | 89.16   | 94.43   |
| 9 | 93.75  | 89.06   | 89.55   | 91.41   | 91.60   | 82.90   | 91.63   |
| 10| 93.75  | 95.31   | 95.24   | 94.53   | 94.49   | 89.07   | 94.49   |

**MSD (N(2))**: 94.22 ± 1.05

|   | $N(3)$ | $\nu^1$ | $\nu^2$ | $\nu^3$ | $\nu^4$ | $\nu^5$ | $\nu^6$ | $\nu^7$ |
|---|--------|---------|---------|---------|---------|---------|---------|---------|
| 1 | 96.88  | 92.19   | 92.54   | 94.53   | 94.66   | 89.16   | 94.68   |
| 2 | 95.31  | 93.75   | 93.85   | 94.53   | 94.57   | 89.07   | 94.58   |
| 3 | 93.75  | 93.75   | 93.75   | 93.75   | 93.75   | 87.50   | 93.75   |
| 4 | 93.75  | 95.31   | 95.24   | 94.53   | 94.49   | 89.07   | 94.49   |
| 5 | 93.75  | 98.44   | 98.36   | 96.09   | 96.00   | 92.29   | 96.03   |
| 6 | 95.31  | 98.44   | 98.39   | 96.83   | 96.84   | 93.80   | 96.84   |
| 7 | 96.88  | 95.31   | 95.38   | 96.09   | 96.12   | 92.20   | 96.13   |
| 8 | 92.19  | 96.88   | 96.72   | 94.53   | 94.40   | 89.16   | 94.43   |
| 9 | 95.31  | 96.88   | 96.83   | 96.09   | 96.06   | 92.20   | 96.07   |
| 10| 92.19  | 93.75   | 93.65   | 92.97   | 92.91   | 85.95   | 92.92   |

**MSD (N(3))**: 94.53 ± 1.69

|   | $N(4)$ | $\nu^1$ | $\nu^2$ | $\nu^3$ | $\nu^4$ | $\nu^5$ | $\nu^6$ | $\nu^7$ |
|---|--------|---------|---------|---------|---------|---------|---------|---------|
| 1 | 96.88  | 98.44   | 98.41   | 97.66   | 97.64   | 95.32   | 97.64   |
| 2 | 96.88  | 96.88   | 96.88   | 96.88   | 96.88   | 93.75   | 96.88   |
| 3 | 96.88  | 96.88   | 96.88   | 96.88   | 96.88   | 93.75   | 96.88   |
| 4 | 93.75  | 96.88   | 96.88   | 96.88   | 96.88   | 93.75   | 96.88   |
| 5 | 93.75  | 98.44   | 98.36   | 96.09   | 96.00   | 92.29   | 96.03   |
| 6 | 96.88  | 96.88   | 96.88   | 96.88   | 96.88   | 93.75   | 96.88   |
| 7 | 95.31  | 98.44   | 98.39   | 96.09   | 96.00   | 92.29   | 96.03   |
| 8 | 95.31  | 96.88   | 96.83   | 96.09   | 96.06   | 92.20   | 96.07   |
| 9 | 95.31  | 95.31   | 95.31   | 95.31   | 95.31   | 90.63   | 95.31   |
| 10| 96.88  | 96.88   | 96.88   | 96.88   | 96.88   | 93.75   | 96.88   |

**MSD (N(4))**: 96.25 ± 1.32

**Fig. 11.** Grad-CAM result on a covid-19 case.
Table 8
Comparison among N(5–8) over validation set.

| N(5) | $\nu^1$ | $\nu^2$ | $\nu^3$ | $\nu^4$ | $\nu^5$ | $\nu^6$ | $\nu^7$ | $\nu^8$ |
|------|---------|---------|---------|---------|---------|---------|---------|---------|
| 1    | 96.88   | 90.63   | 91.18   | 93.75   | 93.94   | 87.67   | 93.98   |         |
| 2    | 90.63   | 93.75   | 93.55   | 92.19   | 92.06   | 84.42   | 92.08   |         |
| 3    | 93.75   | 92.19   | 92.31   | 92.97   | 93.02   | 85.95   | 93.03   |         |
| 4    | 95.31   | 89.06   | 89.71   | 92.19   | 92.42   | 84.54   | 92.47   |         |
| 5    | 95.31   | 90.63   | 90.04   | 92.97   | 93.13   | 86.03   | 93.15   |         |
| 6    | 90.63   | 90.63   | 90.63   | 90.63   | 90.63   | 81.25   | 90.63   |         |
| 7    | 92.19   | 92.19   | 92.19   | 92.19   | 92.19   | 84.38   | 92.19   |         |
| 8    | 95.31   | 89.06   | 89.71   | 92.19   | 92.42   | 84.54   | 92.47   |         |
| 9    | 89.06   | 93.75   | 93.44   | 91.41   | 91.20   | 82.90   | 91.23   |         |
| 10   | 95.31   | 90.63   | 91.04   | 92.97   | 93.13   | 86.03   | 93.15   |         |
| MSD  | 93.44±2.64 | 91.25±1.68 | 91.48±1.37 | 92.34±0.89 | 92.41±0.98 | 84.77±1.80 | 92.44±0.98 |         |

| N(6) | $\nu^1$ | $\nu^2$ | $\nu^3$ | $\nu^4$ | $\nu^5$ | $\nu^6$ | $\nu^7$ | $\nu^8$ |
|------|---------|---------|---------|---------|---------|---------|---------|---------|
| 1    | 96.88   | 96.88   | 96.88   | 96.88   | 96.88   | 96.88   |         |         |
| 2    | 92.19   | 96.88   | 96.72   | 94.53   | 94.40   | 89.16   | 94.43   |         |
| 3    | 95.31   | 95.31   | 95.31   | 95.31   | 95.31   | 95.31   |         |         |
| 4    | 98.44   | 93.75   | 94.03   | 96.09   | 96.18   | 92.29   | 96.21   |         |
| 5    | 98.44   | 93.75   | 94.03   | 96.09   | 96.18   | 92.29   | 96.21   |         |
| 6    | 95.31   | 95.31   | 95.31   | 95.31   | 95.31   | 95.31   |         |         |
| 7    | 95.31   | 95.31   | 95.31   | 95.31   | 95.31   | 95.31   |         |         |
| 8    | 93.75   | 95.31   | 95.24   | 94.53   | 94.49   | 89.07   | 94.49   |         |
| 9    | 93.75   | 95.31   | 95.24   | 94.53   | 94.49   | 89.07   | 94.49   |         |
| 10   | 95.31   | 95.31   | 95.31   | 95.31   | 95.31   | 95.31   |         |         |
| MSD  | 95.47±2.01 | 95.16±1.15 | 95.19±1.04 | 95.31±0.82 | 95.31±0.86 | 90.66±1.66 | 95.32±0.86 |         |

| N(7) | $\nu^1$ | $\nu^2$ | $\nu^3$ | $\nu^4$ | $\nu^5$ | $\nu^6$ | $\nu^7$ | $\nu^8$ |
|------|---------|---------|---------|---------|---------|---------|---------|---------|
| 1    | 95.31   | 95.31   | 95.31   | 95.31   | 95.31   | 95.31   |         |         |
| 2    | 93.75   | 96.88   | 96.77   | 95.31   | 95.31   | 95.31   |         |         |
| 3    | 96.88   | 93.75   | 93.94   | 95.31   | 95.31   | 95.31   |         |         |
| 4    | 96.88   | 95.31   | 95.38   | 96.09   | 96.12   | 92.20   | 96.13   |         |
| 5    | 95.31   | 95.31   | 95.31   | 95.31   | 95.31   | 95.31   |         |         |
| 6    | 95.31   | 95.31   | 95.31   | 95.31   | 95.31   | 95.31   |         |         |
| 7    | 95.31   | 95.31   | 95.31   | 95.31   | 95.31   | 95.31   |         |         |
| 8    | 98.44   | 95.31   | 95.45   | 96.88   | 96.92   | 93.80   | 96.93   |         |
| 9    | 96.88   | 95.31   | 95.38   | 96.09   | 96.12   | 92.20   | 96.13   |         |
| 10   | 96.88   | 95.31   | 95.38   | 96.09   | 96.12   | 92.20   | 96.13   |         |
| MSD  | 97.66±1.52 | 96.88±2.44 | 96.96±2.21 | 97.27±1.12 | 97.28±1.08 | 94.58±2.17 | 97.30±1.06 |         |

Fig. 12. Grad-CAM result on a normal case.

(a) Original image (b) heat map

S.-H. Wang et al.
(3), we can conclude that rank-based average pooling gives significant better performance than using max pooling in N(2).

Finally, checking N(4) in Table 7 obtained the performance as $\nu_4^{N(4)} = 96.25 \pm 1.32$, $\nu_5^{N(4)} = 97.03 \pm 1.55$, $\nu_6^{N(4)} = 97.03 \pm 1.52$, $\nu_7^{N(4)} = 96.64 \pm 1.11$, $\nu_8^{N(4)} = 96.63 \pm 2.21$, $\nu_9^{N(4)} = 96.63 \pm 1.10$. The increase of performances of BDRMBN of N(4) compared to BDRBN of N(3) indicate that multiple-way data augmentation can help improving the performance of the AI classifier.

### 4.5. Visual explanation

We used Gradient-weighted Class Activation Mapping (Grad-CAM) [49] to visually show why our model, BDRMBN of N(4), can make the decision. Grad-CAM uses the gradient of the classification score with respect to the convolutional features determined by the network in order to understand which parts of the image are most important for classification. The “jet” pseudo-color was used in the heat map. Hence, red colors mean important areas for AI diagnosis, and blue colors mean unimportant areas for AI diagnosis.

Fig. 11 shows the Grad-CAM heat map results of a COVID-19 CCT

### Table 9
Comparison of eight network models.

| Model | $\nu_1$ | $\nu_2$ | $\nu_3$ | $\nu_4$ | $\nu_5$ | $\nu_6$ | $\nu_7$ |
|-------|---------|---------|---------|---------|---------|---------|---------|
| N(1)  | 89.22 ± 2.38 | 92.50 ± 2.31 | 92.31 ± 2.10 | 90.86 ± 1.28 | 90.70 ± 1.31 | 81.82 ± 2.53 | 90.73 ± 1.30 |
| N(2)  | 94.22 ± 1.05 | 94.69 ± 2.47 | 94.71 ± 2.29 | 94.45 ± 1.40 | 94.45 ± 1.34 | 88.93 ± 2.78 | 94.46 ± 1.33 |
| N(3)  | 94.53 ± 1.69 | 95.47 ± 2.14 | 95.47 ± 2.05 | 95.00 ± 1.23 | 94.98 ± 1.23 | 90.04 ± 2.47 | 94.99 ± 1.23 |
| N(4)  | 96.25 ± 1.32 | 97.03 ± 1.55 | 97.03 ± 1.52 | 96.64 ± 1.11 | 96.63 ± 1.10 | 93.30 ± 2.21 | 96.63 ± 1.10 |
| N(5)  | 95.44 ± 2.64 | 91.25 ± 1.68 | 91.48 ± 1.37 | 92.34 ± 0.89 | 92.41 ± 0.98 | 84.77 ± 1.80 | 92.44 ± 0.98 |
| N(6)  | 95.47 ± 2.01 | 95.16 ± 1.15 | 95.19 ± 1.04 | 95.31 ± 0.82 | 95.31 ± 0.86 | 90.66 ± 1.66 | 95.32 ± 0.86 |
| N(7)  | 96.09 ± 1.33 | 95.31 ± 0.74 | 95.36 ± 0.67 | 95.70 ± 0.55 | 95.72 ± 0.57 | 91.42 ± 1.11 | 95.72 ± 0.57 |
| N(8)  | 97.66 ± 1.52 | 96.88 ± 2.44 | 96.96 ± 2.21 | 97.27 ± 1.12 | 97.28 ± 1.08 | 94.58 ± 2.17 | 97.30 ± 1.06 |

### Table 10
Performance of proposed N(8) FGCNet on test set.

| Run | $\nu_1$ | $\nu_2$ | $\nu_3$ | $\nu_4$ | $\nu_5$ | $\nu_6$ | $\nu_7$ |
|-----|---------|---------|---------|---------|---------|---------|---------|
| 1   | 98.96   | 96.88   | 96.94   | 97.92   | 97.94   | 95.85   | 97.94   |
| 2   | 96.88   | 96.88   | 96.88   | 96.88   | 96.88   | 93.75   | 96.88   |
| 3   | 96.88   | 98.96   | 98.94   | 97.92   | 97.89   | 95.85   | 97.90   |
| 4   | 96.88   | 95.83   | 95.88   | 96.35   | 96.37   | 92.71   | 96.37   |
| 5   | 96.88   | 95.83   | 95.88   | 96.35   | 96.37   | 92.71   | 96.37   |
| 6   | 97.92   | 95.83   | 95.92   | 96.88   | 96.91   | 93.77   | 96.91   |
| 7   | 95.83   | 95.83   | 95.83   | 95.83   | 95.83   | 91.67   | 95.83   |
| 8   | 100.00  | 97.92   | 97.96   | 98.96   | 98.97   | 97.94   | 98.97   |
| 9   | 96.88   | 93.75   | 93.94   | 95.31   | 95.38   | 90.67   | 95.40   |
| 10  | 100.00  | 97.92   | 97.96   | 98.96   | 98.97   | 97.94   | 98.97   |
| MSD | 97.71 ± 1.46 | 96.56 ± 1.48 | 96.61 ± 1.43 | 97.14 ± 1.26 | 97.15 ± 1.25 | 94.29 ± 2.52 | 97.16 ± 1.25 |
slice. On the left part of Fig. 11(a), the red circle delineated the lesions, where we can see the GGO occurs. Fig. 11(b) show the corresponding heat map. We can see here AI pay the most attention on the GGO lesion (See the red circle on the Fig. 11a), indicating AI successfully capture the GGO lesions. Secondly, AI pay somewhat attention on the tracheae (in the middle of the Fig. 11b), where we can see the GGO occurs. Fig. 11(b) show the corresponding grayscale values of the tracheae tissues, where we can see yellow blots on the middle areas in Fig. 11(b).

Fig. 12 shows the Grad-CAM heat map of a normal CCT slice. Our AI model scans through the whole image and does not find any strong activations (suspicious areas). Hence, the AI model judges this image "healthy".

### 4.6. Effect of deep feature fusion

We compared the performance of using deep feature fusion against not using deep feature fusion. The comparison was done on the validation set. The results using N(5–8) are presented in Table 7. Comparing Tables 5 and 6, we can find that using DFF can increase the classification performance.

For clear view, the results using all the proposed eight models are presented in Table 9, N(1–4) did not use DFF while N(5–8) added DFF to the corresponding networks (See Table 3). Fig. 13 shows the mean and standard deviation of the eight neural network models.

Comparing DBRMBN of N(4) against DBRMBN of N(8), we can see that adding DFF can improve all the five indicators ($\mu^1$, $\mu^2$, $\mu^3$, $\mu^4$, $\mu^5$) except ($\mu^2$, $\mu^5$). This indicates the DFF is effective in increasing the classifier’s performance.

The same scenario can be observed by comparing BN of N(1) against DBN of N(5), comparing BDBN of N(2) DBDBN of N(6), and comparing BDRBN of N(3) and DBRBN of N(7). The reason why DFF can improve the performance is because DFF fuses features from GCN, which learns the relation-awareness relationships (RARs) among the validation images. Hence, classifiers with DFFs were more accurate than those without DFFs.

Besides, from Table 9 and Fig. 13, we can find the optimal $n^* = 8$. That means, N(8) achieved the best performance among all our proposed eight network models. This falls within our expectation, because DBRMBN of N(8) fuses RAR features from GCN with features from DBRMBN of N(4). This feature fusion helps our classifier obtained the best performance. As designed in Section 3.6, the best model among all eight proposed networks is dubbed as FGNet, indicating the fusion of GCN and CNN networks.

### 4.7. Comparison to state-of-the-art approaches

Above performances ran on the validation set. Now we run the best model FGNet, i.e., DBRMBN model on the test set, and report its performance. The results are shown in Table 10. As is shown, $\nu^1_{DB}= 97.14 \pm 1.26$, $\nu^2_{DB}= 97.15 \pm 1.25$, $\nu^3_{DB}= 94.29 \pm 2.52$, $\nu^4_{DB}= 97.16 \pm 1.25$. Comparing Tables 9 and 10, we observe that the performances on validation set and test set are quite similar, only the test performance is slightly less than the validation performance.

We compared our DBRMBN method, i.e., N(8) model, with 15 state-of-the-art approaches: RBFFNN [4], KELM [5], ELM-BA [6], RCBBO [7], 6L-CLF [8], GoogLeNet [9], ResNet-18 [10], RN-50-AD [11], SMO [12], CSSNet [13], GGNet [14], COVNet [15], NiNet [16], FCONet [17], and

| Approach     | $\mu^1$ | $\mu^2$ | $\mu^3$ | $\mu^4$ | $\mu^5$ | $\mu^6$ | $\mu^7$ |
|--------------|---------|---------|---------|---------|---------|---------|---------|
| KELM         | 57.29   | 61.46   | 59.83   | 59.38   | 58.46   | 18.81   | 58.46   |
| ELM-BA       | 57.08   | 62.40   | 67.48   | 64.74   | 61.75   | 19.90   | 61.76   |
| RCBBO        | ±1.86   | ±3.03   | ±1.65   | ±2.26   | ±2.45   | ±2.24   | ±1.66   |
| 6L-CLF [8]   | ±2.90   | ±2.21   | ±1.27   | ±0.85   | ±1.13   | ±1.73   | ±1.15   |
| GoogLeNet [9]| ±3.19   | ±2.14   | ±1.78   | ±2.00   | ±1.27   | ±0.86   | ±1.86   |
| ResNet-18 [10]| ±3.92  | ±2.29   | ±1.58   | ±1.40   | ±1.92   | ±2.62   | ±1.91   |
| KELM         | 59.38   | 58.46   | 18.81   | 58.46   | 58.46   | 18.81   | 58.46   |
| ELM-BA       | 61.75   | 61.75   | 29.90   | 61.76   | 61.76   | 29.90   | 61.76   |
| RCBBO        | ±2.26   | ±2.45   | ±2.24   | ±2.45   | ±2.24   | ±2.24   | ±2.24   |
| 6L-CLF [8]   | ±1.13   | ±1.73   | ±1.73   | ±1.73   | ±1.73   | ±1.73   | ±1.73   |
| GoogLeNet [9]| ±2.00   | ±2.34   | ±2.34   | ±2.34   | ±2.34   | ±2.34   | ±2.34   |
| ResNet-18 [10]| ±2.62  | ±1.15   | ±1.15   | ±1.15   | ±1.15   | ±1.15   | ±1.15   |
| KELM         | ±4.00   | ±4.00   | ±4.00   | ±4.00   | ±4.00   | ±4.00   | ±4.00   |
| ELM-BA       | ±4.00   | ±4.00   | ±4.00   | ±4.00   | ±4.00   | ±4.00   | ±4.00   |
| RCBBO        | ±4.00   | ±4.00   | ±4.00   | ±4.00   | ±4.00   | ±4.00   | ±4.00   |
| 6L-CLF [8]   | ±4.00   | ±4.00   | ±4.00   | ±4.00   | ±4.00   | ±4.00   | ±4.00   |
| GoogLeNet [9]| ±4.00   | ±4.00   | ±4.00   | ±4.00   | ±4.00   | ±4.00   | ±4.00   |
| ResNet-18 [10]| ±4.00  | ±4.00   | ±4.00   | ±4.00   | ±4.00   | ±4.00   | ±4.00   |

Table 11

Comparison with state-of-the-art approaches.
DeCovNet [18]. All the methods were compared on the test set of our 640-image dataset. Some methods were not proposed for detecting COVID-19, some methods work on Chest X-ray images, and some are for multi-class classification, nevertheless, we modified and transferred their methods to our CCT images. The comparison and its plot are presented in Table 11 and Fig. 14. The results in Table 11 and Fig. 14 show that the proposed FGCNet (DBDRMBN) achieved the best results among all algorithms.

5. Conclusions

This paper proposed a total eight network models for COVID-19 detection in CCTs. Our experiments showed our DBDRMBN of N(8) can achieve the best performance among all the eight proposed models. This model is also named as FGCNet for short, and it obtains superior results to other 15 state-of-the-art approaches.

The reason why our FGCNet has the best performance is (i) because the FGCNet (DBDRMBN) is a deep feature fusion combination of an improved CNN model N(4) of BDRMBN and a GCN model. Here, N(4) (BDRMBN) helps to extract learnt individual image-level representations, while GCN helps to extract learnt relation-aware representation. Finally, the DFF strategy help fuse those two types of features. (ii) The proposed N(4) (BDRMBN) is a novel neural network trained with its structure developed and weights trained from scratch. Besides, BDRMBN used several advanced techniques, such as batch normalization, dropout, rank-based average pooling, and multiple-way data augmentation.

The shortcomings of this proposed FGCNet can only handles CCT images. For chest X-ray images and other sources of data, the FGCNet may not work correctly. So, it is necessary to define a network that can fuse different sources/modalities of data and give an overall decision. Another shortcoming is this proposed FGCNet is not verified by a strict clinical test.

The future work directions are: (i) Expand the dataset and test our algorithm on different sources of COVID-19, such as the combination of X-ray and CT. (ii) Test other fuse strategies of CNN and GCN. (iii) Try to employ deeper GCN, and test whether deeper GCN will help improve the performance.

CRediT authorship contribution statement

Shui-Hua Wang: Conceptualization, Methodology, Software, Validation, Data curation, Writing - original draft, Data curation. Vishnu Varthanan Govindaraj: Formal analysis, Writing - original draft, Writing - review & editing. Juan Manuel Górriz: Writing - original draft, Writing - review & editing, Supervision, Funding acquisition. Xin Zhang: Writing - original draft, Writing - review & editing, Supervision, Project administration, Funding acquisition. Yu-Dong Zhang: Resources, Formal analysis, Investigation, Data curation, Writing - review & editing, Supervision, Funding acquisition.

Declaration of Competing Interest

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

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Table 12
Abbreviation list.

| Abbreviation | Full name                               |
|--------------|-----------------------------------------|
| CCT          | chest computed tomography               |
| GGO          | ground-glass opacity                    |
| CAP          | community acquired pneumonia            |
| HS           | hyperspectral                           |
| CNN          | convolutional neural network            |
| GCN          | graph convolutional network             |
| IIR          | individual image-level representation   |
| RAR          | relation-aware representation           |
| MV           | majority voting                         |
| NLAF         | non-linear activation function          |
| ICS          | internal covariant shift                |
| BAN          | Batch Normalization                     |
| DO           | Dropout                                 |
| L2P          | $l_2$ pooling                           |
| MDA          | Multiple-way data augmentation          |
| SSD          | small-size dataset                      |
| LG           | lack of generation                      |
| KMC          | $k$-means clustering                    |
| kNN          | $k$-nearest neighbors                   |
| BN           | Base Network                            |
| FGCNet       | Fusion of GCN and CNN Network           |

Appendix B

Table 13
Symbol list.

| Symbol | Meaning                                |
|--------|----------------------------------------|
| $L$    | Labeling from each individual expert   |
| $\hat{L}$ | Final labeling                       |
| $U$    | Dataset                                |
| $U_1$  | Raw dataset                            |
| $U_5$  | Preprocessed dataset                   |
| $|U|$   | Number of samples in the dataset       |
| $X'$   | Training set                           |
| $X^*$  | Validation Set                         |
| $Y$    | Test set                               |
| $\mu_{\text{min}}$ | Min grayscale value                  |
| $\mu_{\text{max}}$ | Max grayscale value                  |
| $W$    | Width                                  |
| $H$    | Height                                 |
| $C$    | Channel                                |
| $\alpha_s$ | Stability factor                   |
| $\alpha_{\text{rp}}$ | Retention probability                |
| $\mu_e$ | Empirical mean                        |
| $\phi_e$ | Empirical variance                    |
| $\mu_p$ | Population mean                       |
| $\phi_p$ | Population variance                   |
| $\Psi$ | Region to be pooled                   |
| $n$    | Pooling size.                          |
| $P$    | Pooling output                         |
| $a_{\text{g}}$ | Rank threshold                       |
| $\chi$ | Various data augmentation factor       |
| $\eta_{\text{mda}}$ | Number of MDA techniques               |
| $\eta_n$ | Number of new images generated for each DA |
| $a_z$  | Maximum shift factor                   |
| $\eta_{\text{ef}}$ | Enhance factor                     |
| $u_c$  | Number of conv layers                  |
| $u_f$  | Number of FCL layers                   |
| $|V|$  | Cluster centroids                      |
| $W$    | Number of runs                         |
| $w$    | Run index                              |
Appendix C

Fig. 4 shows a simplistic CNN example with four FCL layers. Suppose we have $C(k)$: $k = 1.2.3.4$neurons at $k$-th layer, and assume $C(1) = 6$, $C(2) = 10$, $C(3) = 6$, $C(4) = 4$. Thus, we have in total $\sum_{k=1}^{4} N(k) = 26$ nodes. Suppose we do not consider incoming and outgoing weights, and do not consider the number of biases, the size of learnable weights $C(i,j)$, where $(i,j) = ((1,2),(2,3),(3,4))$ as number of weights between layer $i$ and layer $j$ before dropout, roughly calculating, can be written as $C(1,2) = 6 \times 10 = 60$, $C(2,3) = 10 \times 6 = 60$, $C(3,4) = 6 \times 4 = 24$. In total, we have the total number of learnable weights before dropout as $C = \sum_{i=1}^{4} C(i,j) = 144$.

Using $\alpha_p = 0.5$, the size of learnable weights after dropout between layer $i$ and layer $j$ is $C(i,j) = 2^{\alpha_p} C(i,j)$, which we can calculate the total number of learnable weights as $C^{\rho} = \sum_{i=1}^{4} C(i,j) = 15 + 15 + 6 = 36$. The compression ratio of learnable weights (CRLW), roughly, can be calculated by $C^{\rho}/C = 36/44 = 0.25$.

Appendix D

Using Fig. 5 as a simplistic example, and assuming the region $\Phi(1,1)$ at 1st row 1st column of the input is chosen. For the sake of format, we use its row-vector $\Psi(1,1) = (\Phi(1,1))$ to represent in this paragraph, so we have $\Phi(1,1) = (2.5.1.6.1.1)$. We can calculate the results of L2P as $P^{\text{L2P}}(\Phi(1,1)) = \sqrt{\text{tr}(2.5^2 + 1.6^2 + 1.1^2))/4} = \sqrt[4]{35.02}/4 = 8.75 = 2.96$. The pooling result of AP is $P^{\text{AP}}(\Phi(1,1)) = \text{average}(\Phi(1,1)) = (2.5 + 5 + 1.6 + 1.1) = 4.25$. The MP result is $P^{\text{MP}}(\Phi(1,1)) = \max(\Phi(1,1)) = \max(2.5, 1.6, 1.1) = 2.5$. The rank matrix of $\Phi(1,1)$ also expressed in row-vector format $\Phi(1,1) = \Phi(1,1)$, we have $R_{\Phi(1,1)} = (1.2.3.4)$. The RAP result is $P^{\text{RAP}}(\Phi(1,1)) = (2.5 + 5) = 2 = 3.75$.

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