Dark decay of the neutron

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New decay channels for the neutron into dark matter plus other particles have been suggested for explaining a long-standing discrepancy between the neutron lifetime measured from trapped neutrons versus those decaying in flight. Many such scenarios are already ruled out by their effects on neutron stars, and the decay into dark matter plus photon has been experimentally excluded. Here we explore the decay into a dark Dirac fermion $\chi$ and a dark photon $A'$, which can be consistent with all constraints if $\chi$ is a subdominant component of the dark matter. Neutron star constraints are evaded if the dark photon mass to coupling ratio is $m_{A'}/g' \lesssim (45-60)$ MeV, depending upon the nuclear equation of state. $g'$ and the kinetic mixing between $U(1)'$ and electromagnetism are tightly constrained by direct and indirect dark matter detection, supernova constraints, and cosmological limits.

I. INTRODUCTION

Recently a long-standing experimental discrepancy in the lifetime of the neutron has been highlighted: the decay rate of neutrons stored in a bottle \cite{11,12,13,14,15} seems to be larger than that determined by detecting the decay products from neutrons in flight \cite{16,17,18}. The difference in the associated lifetimes is $\sim 8$ s with a $4\sigma$ tension. Ref. \cite{19} pointed out that this could be explained by a hitherto undetected extra decay channel into dark particles, if the neutron mixes with fermionic dark matter (DM) $\chi$ whose mass is in a narrow range $m_p - m_e < m_\chi < m_n$ consistent with proton stability. The simplest decay channel, $n \to \chi \gamma$, comes from the transition magnetic moment interaction $\bar{n}\sigma_{\mu\nu}\chi F^{\mu\nu}$ induced by the $n$-$\chi$ mixing. This has already been ruled out by a null search for the monochromatic photon \cite{20}. (It was also argued that any such solution of the lifetime problem would exacerbate tensions in discrepant determinations of the neutron axial-vector coupling $g_A$ \cite{21}).

Even if the new decay channel is completely invisible, for example $n \to \chi \phi$ where $\phi$ is a dark scalar, neutron stars ostensibly rule out the scenario \cite{22,23,24}, since $\chi$ typically has a much softer equation of state than nuclear matter at high density. The conversion of $n$ to $\chi$ in a neutron star (NS) then leads to the maximum possible mass of the star being well below the largest values observed (near $2M_\odot$). Ref. \cite{22} pointed out that this constraint can be evaded if $\chi$ has additional pressure from the repulsive self-interactions that would come from dark photon ($A'$) exchange, if the mass-to-coupling ratio $m_{A'}/g'$ is sufficiently large, though the minimum required value was not determined. One of our goals is to find this value.

This suggests that a consistent picture can be made if the new dark decay channel is $n \to \chi A'$. Astrophysical and cosmological considerations substantially constrain DM in the mass range required to explain the neutron lifetime anomaly. However, $\chi$ could still be a subdominant component of the total dark matter.

In the following, we start by deriving constraints on our scenario that depend only upon the low-energy particle content at the GeV scale or below, in Section II. This is followed by analysis of the effects upon neutron stars, Sec. III \cite{25} where an upper bound on $m_{A'}/g'$ is derived. We introduce the microscopic renormalizable model in Sec. IV and discuss the implications for cosmology in Sec. V \cite{26}. The constraints from direct and indirect detection are derived in Sections VI and VII \cite{27}. Various constraints on the kinetic mixing parameter between the $U(1)'$ and electromagnetic $U(1)$ field strengths are compiled in Sec. VIII \cite{28} followed by our conclusions, Sec. IX.

II. MODEL-INDEPENDENT ANALYSIS

Before presenting a more complete particle physics model, we start with the low-energy effective Lagrangian that contains almost everything needed for the phenomenology. It has mixing of the Dirac $\chi$ with the right-handed component of the neutron (this restriction does come from UV considerations, to be explained later) and the usual terms for $\chi$ interacting with a dark photon $A'$:

$$\mathcal{L}_{\text{eff}} = \bar{\chi}(i\gamma^\mu - m_\chi)\chi + \bar{n}(i\gamma^\mu - m_n + \mu_n\sigma^{\mu\nu}F_{\mu\nu})n - \frac{1}{2}F'_{\mu\nu}F'^{\mu\nu} - \frac{1}{2}m_A' A'^\mu A'_\mu - \delta m \bar{n}\chi L + \text{h.c.} - \frac{\epsilon}{2} F_{\mu\nu}F'^{\mu\nu}$$

(1)

where $D_\mu = \partial_\mu - ig' A'_\mu$ and $\mu_n$ is the neutron magnetic dipole moment. Kinetic mixing with the photon is included so that $A'$ will eventually decay to photons through a loop diagram, or electrons if $m_{A'} > 2m_e$. We assume that $\chi$ is a Dirac particle, since UV models in which $\chi$ is Majorana generically lead to dinucleon decays such as $^{16}\text{O}(pp) \to ^{14}\text{C}\pi^+\pi^-$. \cite{29}

Diagonalization of the $n$-$\chi$ mass matrix requires rotations of $(n_R, \chi_R)$ and $(n_L, \chi_L)$ respectively by angles $\theta_R$ and $\theta_L$ with

$$\theta_R \equiv \frac{m_n \delta m}{m_n - m_\chi}, \quad \theta_L \equiv \frac{m_\chi \delta m}{m_n - m_\chi}$$

(2)
Since $m_\chi$ is close to $m_n$, these angles are roughly equal, \( \theta = \theta_R \approx \theta_L \approx \delta m / (2(m_n - m_\chi)) \). Going to the mass basis, the \( \tilde{\chi}A'\chi \) interaction then leads to an off-diagonal term,

\[
- g'\theta \tilde{n}A'\chi + \text{h.c.} \tag{3}
\]

that leads to the dark decay \( n \to A' \) assuming that \( m_n > m_\chi + m_{A'} \). Since \( A' \) is unstable because of kinetic mixing with the photon, we assume that it is either sufficiently long-lived to escape detection, or its decay products \( e^+e^- \) or \( 3\gamma \) have not yet been excluded by observations of neutron decay.

The decay rate for \( n \to \chi A' \) can be expressed in terms of the ratios \( x = (m_n - m_\chi)/m_n \) and \( r = m_{A'}/(m_\chi - m_n) \), where \( x \in [0, 1.78 \times 10^{-3}] \) (the upper limit is imposed by the stability of \(^9\text{Be} \) in \([8, 15]\)) and \( r \in [0, 1] \):

\[
\Gamma(n \to \chi A') \cong \frac{g'^2\theta^2 m_n x}{2\pi r^2} (1 - r^2)^{3/2} \cong \frac{g'^2(\delta m)^2 m_n}{8\pi m_{A'}^2} x(1 - r^2)^{3/2} \tag{4}
\]

where we have ignored negligible higher order corrections in \( x \), and in the second line eliminated \( \theta \) using \([2]\). The limit \( m_{A'} \to 0 \) is not singular, despite appearances, when \( A' \) gets its mass from spontaneous symmetry breaking, as we explicitly show in section \([IV]\) \( g'\delta m/m_{A'} \) remains finite in this limit.

To resolve the neutron lifetime discrepancy, the partial width must be \( 7 \times 10^{-30} \text{ GeV} \) \([8]\). For definiteness, we adopt the reference value \( m_\chi = 937.9 \text{ MeV} \), which maximizes the dark decay rate with \( m_n - m_\chi \cong 1.67 \text{ MeV} \). Moreover we consider two benchmark values of \( m_{A'} = 1.35 \text{ MeV} \) and 0.5 MeV to illustrate the differences between being above or below the \( 2m_e \) threshold for \( A' \) decays. We refer to the two cases as scenarios \( A \) and \( B \), respectively. We then find

\[
g'\delta m / m_{A'} \cong 7.2(3.5) \times 10^{-13}, \quad \text{scenario A (B)} \tag{5}
\]

With the neutron star bound \( m_{A'}/g' \lesssim 60 \text{ MeV} \) to be derived in section \([III]\) this implies \( \delta m < 4(2) \times 10^{-11} \text{ MeV} \), which gives a limit on the mixing angle

\[
\theta < 1.3 \times 10^{-11} (6.3 \times 10^{-12}) \tag{6}
\]

for the two scenarios. Although the decay \( \chi \to pe^-\bar{\nu}_e \) is kinematically allowed if \( m_\chi > m_p + m_e^- = 938.8 \text{ MeV} \), such a small mixing endows \( \chi \) with a lifetime well beyond the age of the universe. Therefore \( \chi \) is always a component of the DM, even when it is not absolutely stable.

To satisfy the constraint on \( n \to \chi\gamma \) from \([9]\), \( \delta m \) must be smaller by a factor of approximately 2.6 than the value needed for explaining the lifetime discrepancy in terms of this decay\([1]\). Using the value of \( \delta m \) determined

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1 Ref. \([9]\) does not quite exclude the model with minimum \( m_\chi = 937.9 \) that we consider, which would lead to a photon of energy 1.66 MeV. The maximum photon energy excluded in \([9]\) is 1.62 MeV. We assume that this narrow window will be closed by a wider search.
how large \( m_{A'}/g' \) can be while still attaining a 2 solar mass neutron star.

We have followed the procedure outlined in [11] to answer this question. The DM is treated as a degenerate Fermi gas with self-interactions, so that its energy density is given by

\[
\rho_\chi = \frac{1}{\pi^2} \int_0^{k_F} dk^2 \sqrt{k^2 + m_\chi^2} + \frac{g'^2}{2m_{A'}} n_\chi^2 \tag{9}
\]

where \( k_F \) is the Fermi momentum and \( n_\chi = k_F^3/3\pi^2 \). \( k_F \) is determined by the chemical potential

\[
\mu_\chi = \sqrt{k_F^2 + m_\chi^2} + \frac{g'^2}{2m_{A'}} n_\chi \tag{10}
\]

The DM pressure is given by \( p_\chi = -\rho_\chi + \mu_\chi n_\chi \). Chemical equilibrium implies that \( \mu_\chi \) equals the baryon (neutron) chemical potential \( \mu_B \), which is determined by the nuclear equation of state (EoS). \( \chi \) will be produced at any radius within the NS where \( \mu_B > m_\chi \). The DM contributions to pressure and energy density are added to those of the nuclear matter to find the modified EoS.

The nuclear EoS can be specified in terms of the dimensionless nuclear density \( \rho \), as a function of the dimensionless nuclear density \( x = n_c/n_\rho \), where \( n_0 = 0.16 \text{ fm}^{-3} \) is the saturation density. We adopt a polytropic EoS of the form [19]

\[
E_n(x) = ax^\alpha + bx^\beta \tag{11}
\]

that has been fit to the results of quantum Monte Carlo calculations incorporating realistic 3-nucleon forces. The nuclear pressure is given by \( p_n = n_0^2 dE_n/dn = n_0 (ax^\alpha + bx^\beta) \), and the energy density is \( \epsilon_n = n_c (m_n + E_n) \). The chemical potential is then \( \mu_B = (p_n + \epsilon_n)/n_\rho \). This approximation is adequate at high densities near the center of the NS, but at some radius as the density increases, the effect of nuclear binding becomes important, allowing \( \mu_B \) to fall below \( m_\chi \) (which otherwise would not happen) and also \( \mu_\chi \). At this radius the \( \chi \) density falls to zero and the dark matter can no longer soften the EoS. We model this effect by subtracting the binding energy \( E_b = 8 \text{ MeV} \) (which follows from the semi-empirical mass formula of nuclear physics [20]) from \( \mu_B \).

Carrying out the above procedure we find the NS mass as a function of its radius for a range of central densities of the NS, to produce the mass-radius curves corresponding to different values of \( m_{A'}/g' \). The results are shown in fig. 1 for several equations of state from ref. [19]. The solid lines (labeled \( V_{3\pi} + V_F \)) correspond to a moderately stiff EoS with \( a(b) = 13.0(3.21) \text{ MeV} \), \( \alpha(\beta) = 0.49(2.47) \), while the dashed ones (labeled U1X) pertain to a more stiff EoS with \( a(b) = 13.4(5.62) \text{ MeV} \), \( \alpha(\beta) = 0.514(2.436) \). The dotted curves (labeled \( V_{3\pi}^{PW} + V_R^{PW} \)) are for a soft EoS that cannot produce a 2\( M_{\odot} \) NS even in the absence of dark matter. To obtain a maximum mass compatible with 2\( M_{\odot} \) requires

\[
\frac{m_{A'}/g'}{g'} \lesssim (45 - 60) \text{ MeV} \tag{12}
\]

depending upon the nuclear EoS.

### IV. UV MODEL

Direct and indirect signals of subdominant \( \chi \) dark matter can depend upon details of the particle physics beyond the low-energy effective description [1]. In particular a light scalar particle must be in the spectrum, to account for the mass of \( A' \) through the Higgs mechanism. Here we build a minimal model that could consistently give rise to the Lagrangian [1]. It is strongly constrained by the gauge symmetries, giving us little freedom in its construction. We demand that the U(1)' gauge symmetry be only spontaneously broken, requiring a scalar \( \phi \) that carries U(1)' charge, with a potential

\[
V = \lambda (|\phi|^2 - v^2)^2 \tag{13}
\]

Moreover a renormalizable interaction of \( \chi \) with a quark needs a scalar \( \Phi_1 \) that is fundamental under SU(3) and also charged under U(1)'. To connect this to the other quarks in the neutron, a second triplet scalar \( \Phi_2 \), neutral under U(1)' is needed, along with a cubic scalar interaction,

\[
\mu \Phi_{1,a} \Phi_2^{a*} \phi \tag{14}
\]

where \( \mu \) has dimensions of mass. To satisfy SU(2)_L gauge symmetry we take the triplets to couple only to right-handed quarks,

\[
\lambda_1 \bar{d}^c P_L \Phi_{1,a} + \lambda_2 \epsilon^{abc} \bar{u}^c_R d_5 \Phi_{2,c} \tag{15}
\]

\( \Phi_1^* \), \( \chi \) and \( \phi \) all carry unit dark \( U(1)' \) charge with coupling \( g' \). The vacuum expectation value (VEV) of \( \phi \) breaks \( U(1)' \) and gives the dark photon mass \( m_{A'} = g'v' \).

We can consistently assign baryon number to all the new fields: \( B_c = 1 \), \( B_{\Phi_1} = B_{\Phi_2} = -2/3 \), \( B_\phi = 0 \). Therefore the model is free from constraints on B-violating processes such as neutron-antineutron oscillations and dimuon decay. We need to kinematically forbid decays of \( ^9\text{Be} \) (if \( m_{\chi} \geq 937.9 \text{ MeV} \) also stabilizes the proton and forbids possibly problematic decays of \( \Lambda \) baryons to final states including a \( \chi \), such as \( \Lambda_0 \rightarrow \chi K_0 \), as well as decays of light mesons to \( \chi \)).

The virtual exchange of the heavy \( \Phi_2 \) generates a contact interaction that can be Fierz-transformed to

\[
\mathcal{L}_c = \frac{|\lambda_1|^2}{2m_{\Phi_2}} (\bar{u}_R \gamma_\mu u_R) (\bar{d}_R \gamma^\mu d_R) \tag{16}
\]

The coefficient is constrained by measurements of dijet angular distributions at the LHC [21], \( m_{\Phi_2}/\lambda_2 \gtrsim 4 \text{ TeV} \). The scalar triplets, which could decay to two jets or a jet and missing energy, must be at the TeV scale to satisfy LHC constraints on their direct production. [22] Integrating them out generates the effective interaction

\[
\eta \bar{u} \phi^* P_L \chi \tag{17}
\]
with

\[
\eta = \frac{\beta \mu \lambda_1 \lambda_2}{m_{\Phi_1} m_{\Phi_2}} \cong 2.4 \times 10^{-12} \left( \frac{\lambda_1 \lambda_2 \mu}{\text{TeV}} \right)
\]  

(18)

where \( \beta \approx 0.014 \text{GeV}^3 \) from lattice QCD \[23\], and the scalar masses saturate the ATLAS limit \( m_{\Phi_i} > 1.55 \text{ TeV} \). When \( \phi \) gets its VEV, the off-diagonal mass \( \delta m = \eta' \) between \( n_R \) and \( \chi_L \) is generated. Since \( m_{A'/g'} \ll \eta' \), we can combine (18) with (5) to determine

\[
\lambda_1 \lambda_2 \mu \cong (140 - 290) \text{ GeV}
\]

(19)

If \( \lambda_1 \sim \lambda_2 \sim 0.4 \) (consistent with the previous LHC limits), then \( \mu \) can be near the TeV scale, like the triplet scalar masses. But \( \eta' \) must be at the much lower scale \( \lesssim 60 \text{ MeV} \) from (12).

The scalar \( \phi \) cannot be arbitrarily heavy. Its mass is \( m_{\phi} = 2\sqrt{\lambda} v \) hence \( m_{\phi}/\lambda_{A'} = 2\sqrt{\lambda}/g' \). The upper limit from partial wave unitarity is \( \lambda \leq 4\pi \). For our benchmark models this would give a mass of order \( m_{\phi} \sim 70 \text{ MeV} \). The decay channel \( n \to \chi \phi \) is closed, and only leads to a subdominant mode \( n \to \chi A' A' \) through virtual \( \phi \) exchange. However, when \( m_{\phi} \gg m_{A'} \), the scalar decays via \( \phi \to A' A' \), and as \( \chi \chi \to \phi A' \) is an allowed process, it can have non-negligible effects on both cosmology and indirect detection signals. For simplicity we assume that \( \lambda \) is large and \( m_{\phi} \) takes the benchmark value of 70 MeV. This is large enough so that we can ignore the effects of \( \phi \) on neutron decay, but we will consider its effect on DM physics. We also note the cubic coupling (14) could lead to interesting cascade decays of the heavier of the two color triplet scalars \( \Phi_i \) produced at the LHC, but this is beyond the scope of the present work.

### V. Cosmology

In the limit of low relative velocity, the cross section for \( \chi \chi \) elastic scattering by dark photon exchange takes the form

\[
\sigma_{\chi \chi} = \frac{g'^4 m_{\chi}^2}{4 \pi m_{A'}^2} \gtrsim 2 \times 10^{-24} \text{ cm}^2,
\]

(20)

with the lower bound derived using the limit on \( m_{A'}/g' \) from neutron stars in Eqn. (12). It is interesting that the lowest allowed value of \( \sigma_{\chi \chi} \) is of the appropriate strength to explain observations of astrophysical structure on small scales that are in tension with the predictions of cold dark matter \[24\]. However, constraints from the Cosmic Microwave Background (CMB) and astrophysics discussed in Section VII will ultimately limit \( \chi \) to be a small fraction of the total DM, preventing our model from addressing these issues. Larger values of \( \sigma_{\chi \chi} \) could run a foul of constraints on DM self-scattering from the Bullet Cluster \[26\], but this limit is avoided when \( \chi \) is subdominant; up to around 10% of the total DM population might have such strong self-interactions \[27\].

The relic density of \( \chi \) is determined by \( \chi \bar{\chi} \to A' A' \) and \( \chi \bar{\chi} \to \phi A' \) annihilations, assuming there is no asymmetry between \( \chi \) and \( \bar{\chi} \). There are also a tree level process that give annihilation into quarks, \( \chi \bar{\chi} \to d \bar{d} \), but this process is greatly suppressed by the TeV scale mass of the \( \Phi_2 \). The cross sections for the relevant processes are given by \[29\].

## References

\[2\] For a more complicated dark sector model which could explain both the neutron lifetime puzzle and small scale structure issues, see \[29\].

\[
\langle \sigma_{\text{ann}} \rangle_{\chi \bar{\chi} \to A' A'} = \frac{g'^4}{16 \pi m_{\chi}^2} \left( 1 - \eta_{A'} \right)^{3/2} \left( 1 - \eta_{A'}/2 \right)^2
\]

(21)

\[
\langle \sigma_{\text{ann}} \rangle_{\chi \bar{\chi} \to \phi A'} = \frac{g'^4}{4096 \pi m_{\chi}^2} \frac{\sqrt{(\eta_{\phi} - \eta_{A'})^2 - 16 \eta_{A'} (\eta_{\phi} - \eta_{A'})} + 32 \eta_{A'}^2}{(1 - \eta_{A'}/4)^2},
\]

(22)

where \( \eta_{A' \phi} = m_{A' \phi}^2 / m_{\chi}^2 \). For \( \chi \) to make up all of the DM, the total annihilation cross section should be close to \( 10^{-24} \text{cm}^2/\text{s} \) \[29\]. If \( m_{A'} < m_{\chi} \), \( m_{\phi} = 70 \text{ MeV} \), and \( \chi \) constitutes less than 10% of the total DM, we need a 10 times larger cross section, leading to a lower bound of \( g' > 0.041 \). If this bound were saturated, then the NS limit \[12\] would read \( m_{A'} < 2.5 \text{ MeV} \). For a strong coupling \( g' = 1 \), the \( \chi \) relic density would be \( 3 \times 10^{-7} \) of the total DM density.

Since \( \chi \) is a Dirac particle, it is possible that it has an asymmetry from some unknown mechanism operating in the early universe. Then it would be possible to have large \( g' \) and a more significant fraction of \( \chi \) being the dark matter. Moreover, if the asymmetric component number density happens to be close to the symmetric...
contribution then one CP state of $\chi$ (either $\chi$ or its antiparticle) will have a suppressed density, which could weaken indirect detection constraints. We do not pursue this loophole in the present work, but it should be kept in mind.

$\chi$ and $A'$ chemically decouple at a dark sector temperature of $m_\chi/30 \approx 31$ MeV. At this time the $A'$ are still relativistic with a large number density, which can lead to several problems: if they decay during the time of Big Bang Nucleosynthesis (BBN) their energetic decay products can disturb the production of light nuclei by diluting the baryon-photon ratio as well as causing photodissociation of the nuclei, and decays during and after recombination can distort the CMB temperature fluctuations. Moreover when the dark photons become non-relativistic, an early period of matter-domination can occur which would change the expansion rate of the universe and cause further problems for BBN.

To avoid these issues, we follow [31] and require the dark photons to decay before they exceed half the energy density of the universe. The temperature of the SM photon bath at the time this occurs was shown to be

$$T_{\text{dom}} \approx \frac{4m_{A'}Y_{A'}}{3f}$$

where $Y_{A'} = n_{A'}/s_{SM}$ at $\chi$ freeze-out and $f = 1/2$ is the fraction of the universe’s energy density made up of dark photons. $Y_{A'}$ is given by

$$Y_{A'} = \frac{45\zeta(3)}{2\pi^4} \frac{g_D}{g_{SM}}$$

where $g_D/g_{SM}$ is the ratio of relativistic degrees of freedom in the dark sector to that of the SM sector when the two sectors thermally decouple. As the regions of parameter space we are interested in lead to small scattering cross sections between dark and SM particles, we assume that the two sectors thermally decouple when all species are relativistic, so $g_D = 8$, $g_{SM} = 106.75$, and $Y_{A'} \approx 0.02$. We then require the lifetime $\tau_{A'}$ to be less than $H^{-1}(T_{\text{dom}})$, the inverse Hubble rate at this temperature. This leads to constraints on the kinetic mixing parameter $\epsilon$ that we present in section VIII. We emphasize that the method we have used here to estimate the cosmological constraints on the dark photon lifetime is rough, and more detailed studies similar to those undertaken in [32,33] are needed to determine this limit with greater precision.

Finally, DM annihilation close to recombination can also lead to distortions of the CMB anisotropies. Based on searches for this effect in temperature and polarization data, the Planck collaboration has determined the following 95% CL constraint [50]:

$$f_{\text{eff}} \left( \frac{\Omega_{\chi}}{\Omega_{DM}} \right)^2 \frac{\langle \sigma_{\text{ann}}v_{\text{rel}} \rangle}{m_\chi} < 8.2 \times 10^{-28} \text{ cm}^3/\text{s/GeV}$$

where $f_{\text{eff}}$ is an efficiency parameter that depends on the spectrum of injected electrons and photons, while $\Omega_{DM}$ and $\Omega_{\chi}$ denote the ratio of the energy densities of the total dark matter and $\chi$, respectively, to the critical density. For $m_\chi = 937.9$ MeV, $f_{\text{eff}}$ is approximately 0.5 for DM annihilations to $2e^+e^-$ or $3e^+e^-$ final states, and 0.4 for annihilation to $6\gamma$ or $9\gamma$ final states [37]. Therefore $(\Omega_{\chi}/\Omega_{DM})^2 \langle \sigma_{\text{ann}}v_{\text{rel}} \rangle \lesssim 1.5 \times 10^{-27} \text{ cm}^3/\text{s}$ for scenario A ($A'$ decays to $e^+e^-$), while $(\Omega_{\chi}/\Omega_{DM})^2 \langle \sigma_{\text{ann}}v_{\text{rel}} \rangle \lesssim 1.9 \times 10^{-27} \text{ cm}^3/\text{s}$ for scenario B ($A'$ decays to $3\gamma$).

VI. DIRECT DETECTION

Because of kinetic mixing, $A'$ couples to standard model (SM) particles of charge $e$ with strength $e\epsilon$. The cross section for $\chi$ to scatter on protons is

$$\sigma_{\chi p} = \frac{4\alpha(g'\epsilon)^2\mu_{px}}{m_{A'}^4}$$

where $\mu_{px} = 469$ MeV is the reduced mass of $\chi$ and the proton. The CRESST-III experiment [38] sets a limit of $10^{-38}$ cm$^2$ for scattering on nucleons at $m_\chi \approx 1$ GeV, which is relaxed by a factor of $\sim 2$ for our model where only protons scatter. This leads to the constraint

$$g'\epsilon < 9.85 \times 10^{-11}\left(\frac{m_{A'}}{\text{MeV}}\right)^2\left(\frac{\Omega_{DM}}{\Omega_{\chi}}\right)^{1/2}$$

A similar, but weaker bound, arises from $\chi$-electron scattering, which has been constrained using XENON100 data in ref. [39].

Mixing of $\chi$ with the neutron leads to scattering mediated by the strong interactions of the neutron with nucleons, of order $\theta^2\sigma_{np}$, where $\sigma_{np} \approx 200$ is the low-energy cross section for neutron-proton scattering. In view of [40], $\theta^2\sigma_{np} < 10^{-67}$ cm$^2$, far from observability. In models with $m_\chi > m_n$, as suggested in ref. [41] for evading the NS constraint, an inelastic $\chi N \rightarrow \bar{N}N$ cross section of order $\theta^2\sigma_{np} \sim 10^{-45}$ cm$^2$ would arise, with a highly distinctive signature of large energy deposited in the target material. This is still 7 orders of magnitude below current sensitivity of ordinary elastic scattering, but the large release of energy might make it more observable.

In addition to these contributions that only depend upon the low-energy effective description [4], exchange of the heavy colored scalar $\Phi_1$ in the UV model leads to scattering of $\chi$ on down quarks, which after Fierz-transforming comes from the operator

$$\frac{\lambda_1^2}{2m_{\Phi_1}^2} (\bar{\chi}_L \gamma^\mu \chi_L)(\bar{d}_L \gamma_\mu d_R)$$

3 If $n_\chi > n_{\bar{\chi}}$, we define $n_S = n_S + n_A$ and $n_{\bar{\chi}} = n_S - n_A$, where $n_S$ and $n_A$ are the number densities of the symmetric and antisymmetric components respectively.
The vector part of the quark current is simply related to that of nucleons (counting the number of down quarks in the nucleon). The corresponding cross section is $\lesssim 10^{-40}$ cm$^2$, several orders of magnitude below the current limit.

VII. INDIRECT DETECTION

Indirect DM searches can give strong limits on the annihilation rate of $\chi$ particles. In particular scenario B, where $A' \to 3\gamma$, could lead to significant fluxes of gamma-rays from nearby dwarf spheroidal galaxies, and the Fermi-LAT collaboration has searched for this excess emission [40]. The spectrum of photons from a single decay of an $A'$ (in the rest frame of the $A'$) is given by

$$dN/dE' = \frac{16E'^3}{17m_{A'}} \left[ 1715 - 6210 \frac{E'}{m_{A'}} + 5838 \left( \frac{E'}{m_{A'}} \right)^2 \right]$$

for $0 \leq E' \leq m_{A'}/2$. The spectrum of photons from the annihilation $\chi\bar{\chi} \to A'A'$ (in the center of mass frame of the two annihilating particles) is then given by the boost equation

$$dN/dE = \frac{2}{(x_+ - x_-)} \int_{E_{x_+}}^{E_{x_+}} \frac{dN}{dE'} dE'$$

where $x_\pm = m_\chi/m_{A'} \pm \sqrt{(m_\chi/m_{A'})^2 - 1}$. In principle, annihilations of $\chi\bar{\chi}$ to $\phi A'$ will also have some effect on the shape of the average photon spectrum, but for the regions of parameter space of interest the branching fraction to the $\phi A'$ final state is less than 1/5 (see Eqs. 21 and 22). Therefore we make the approximation that $dN/dE$ is determined solely by annihilations of $\chi\bar{\chi}$ to $A'A'$. With this spectrum we can determine the expected flux from a particular galaxy. Using the gamLike code [42], we calculate a likelihood function based on 6 years of Fermi-LAT observations of 15 dwarf spheroidal galaxies. With this likelihood we find that the quantity $(\Omega_\chi/\Omega_{DM})^2(\sigma_{ann}v_{rel}) < 2.8 \times 10^{-28}$ cm$^3$/s at 95% CL for 6-photon final states.

Scenario A, in which the dark photons decay to electron positron pairs, could in theory give a large flux of positrons which could be detected by Voyager 14 and the AMS-02 [44, 45] experiment. However, it was shown in [46] that significant uncertainties in the model of cosmic-ray propagation make it difficult to reliably constrain dark matter candidates with masses less than a GeV via these observations, so we do not consider them further. Limits can also be placed on the $\chi\bar{\chi}$ annihilation rate in this scenario with Fermi observations of dwarf spheroidal galaxies, but these limits are subdominant to those from observations of the CMB, which we discussed in Sec. V.

VII.1. Constraints on $g'$. As $m_{A'} \ll m_\chi$, the DM annihilation cross section is subject to large Sommerfeld enhancement at small relative velocities. This leads to an enhanced annihilation rate in dwarf spheroidal galaxies and at the time of recombination. The enhanced cross section is given by $\langle \sigma_{ann}v_{rel} \rangle = S(\sigma_{ann}v_{rel})_0$, where $\langle \sigma_{ann}v_{rel} \rangle_0$ is the sum of Eqs. 21 and 22 and the Sommerfeld factor is approximately 50

$$S = \frac{\Gamma(a_-)\Gamma(a_+)/\Gamma(1 + 2iu)}{\beta}$$

with $a_\pm = 1 + iu \left( 1 \pm \sqrt{1 - x/u} \right)$, $x = g'^2/4\pi\beta$, $u = 6m_\gamma/\pi^2m_{A'}$, and $\beta = v_{rel}/c$. For all of the dwarf spheroidal galaxies, we make the approximation $\beta \sim 10^{-4}$ (for a compilation of the velocity dispersions in each dwarf spheroidal of interest, see [51]) and we take $\beta \sim 10^{-8}$ at times around recombination.

Increasing $g'$ ultimately reduces the expected signal in searches for DM annihilation, as the increase in the annihilation rate from the increased cross section is more than offset by the reduced $\chi$ relic density. For scenario A ($A'$ decays to $e^+e^-$), the CMB constraints described in Sec. V limit $g' \gtrsim 0.07$, so $\chi$ can be no more than 1.2% of the total DM, while for scenario B ($A'$ decays to $3\gamma$), $g' > 0.11$. For scenario B, the gamma-ray limits are even stronger, with $g'$ limited to values greater than 0.14. This corresponds to $\chi$ making up only 0.08% of the total DM. These limits are displayed in Fig. 3. Lowering the mass of the dark photon increases the Sommerfeld enhancement and shifts the limits on $g'$ to higher values, as more suppression of the $\chi$ relic density is needed to avoid these constraints.

VIII. KINETIC MIXING CONSTRAINTS

The BaBar experiment has searched for production of $A'$-photon pairs in $e^+e^-$ collisions, with the $A'$ taken to decay to invisible particles [49]. This leads to the constraint $\epsilon < 10^{-3}$. Since the dark photon in our model will decay outside the detector when $\epsilon = 10^{-3}$, this limit applies here. Further direct search limits come from beam dump experiments, where dark photons with mass $\lesssim 2$ MeV can be produced (and detected if $m_{A'} > 2m_\gamma$). Ref. [48] finds a limit of $\epsilon < 2.5 \times 10^{-8}$ from the E137 experiment. In addition, if $A'$ is emitted copiously from supernovae, the observed emission of neutrinos from supernova 1987A would have been attenuated. This robustly excludes the overlapping range $\epsilon \in [2 \times 10^{-9}, 1 \times 10^{-6}]$ [47] (see also [52, 53]). If $m_{A'}$ is below the $2m_\gamma$ threshold, the beam dump limits do not apply, and the supernova limits shift to $\epsilon \in [2 \times 10^{-9}, 8 \times 10^{-6}]$.

A lower bound on $\epsilon$ comes from the requirement that $A'$ decays sufficiently fast (before recombination) so as...
not to disturb the CMB. For scenario A, the width of the
dominant \( A' \to e^+ e^- \) decay and corresponding lifetime
are given by

\[
\Gamma_{e^+ e^-} = \frac{\alpha^2}{3 m_{A'}} (m_{A'}^2 + 2m_e^2) \left( 1 - 4m_e^2/m_{A'}^2 \right)^{1/2},
\]

\[
\tau_{e^+ e^-} \approx 24 \left( \frac{10^{-10}}{\epsilon} \right)^2 \text{s}. \tag{32}
\]

Using the rate for \( A' \to 3\gamma \) from \cite{41}, the lifetime for the
\( A' \) when \( m_{A'} < 2m_e \) is

\[
\tau_{3\gamma} \approx 2 \times 10^{12} \left( \frac{10^{-10}}{\epsilon} \right)^2 \left( \frac{1 \text{ MeV}}{m_{A'}} \right)^9 \text{s}. \tag{33}
\]

The exact upper limit on \( \tau \) from the CMB has not been worked out in detail in the literature; published constraints on the allowed abundance of \( A' \) versus lifetime only go down to \( \tau = 10^{12} \text{s} \), where the constraints are rapidly weakening, but not yet gone; see for example fig. 7 of ref. \cite{54} or fig. 4 of ref. \cite{55}. The true limit is probably somewhat lower than \( 10^{12} \text{s} \); for example if \( \tau_{3\gamma} < 10^{11} \text{s} \) and \( m_{A'} = 0.5 \text{ MeV} \), we require \( \epsilon > 4.5 \times 10^{-10} \), but since this overlaps with the CMB limits shown in Fig. 2 (right), this uncertainty is not important for our constraints.

Concerning limits from BBN, following the argument of section \ref{BBN} the requirement for the lifetime of \( A' \) is \( \tau_{e^+ e^-} < 5400 \text{s} \) for \( m_{A'} = 1.35 \text{ MeV} \) and \( \tau_{3\gamma} < 3920 \text{s} \) for \( m_{A'} = 0.5 \text{ MeV} \). This translates into lower bounds on \( \epsilon \) of \( 2 \times 10^{-11} \) and \( 5 \times 10^{-5} \) for scenarios A and B respectively, as displayed in Fig. 2 along with the other constraints derived in previous sections. These plots show that the combination of direct detection and cosmological constraints strongly disfavor \( m_{A'} < 1.0 \text{ MeV} \)—only when \( A' \) is heavy enough to decay at tree level are the BBN constraints on \( \epsilon \) sufficiently weak for the model to be viable. Lower values of \( m_{A'} \) require much larger \( \epsilon \) to ensure that \( A' \) decays before disturbing BBN.

\section{Conclusions}

The possibility that the neutron decays into a dark fermion \( \chi \) and a dark photon \( A' \) is highly constrained by an array of laboratory and astrophysical observations. The mass of \( \chi \) must lie in a narrow window between 937.9 and 939.6 MeV. The mass of the \( A' \) must be greater than 1.022 MeV (2m_e) and less than 1.67 MeV.\footnote{In an extended model, one might circumvent the lower limit on \( m_{A'} \) by allowing for \( \chi \) to be a long-lived unstable particle with invisible decay products, perhaps including the true dark matter of the universe. Such a framework might be able to circumvent the direct detection constraints that lead to \( m_{A'} < 2m_e \) being excluded in our model.} The U(1)’ gauge coupling cannot be small (above 0.07), implying that \( \chi \) comprises no more than \( \sim 1\% \) of the total DM. The kinetic mixing parameter must lie in a fairly narrow range of \( 10^{-11} \sim 10^{-9} \). It is intriguing that despite the many restrictions, there is still viable parameter space.

The decay mode \( n \to \chi \gamma \) is still present in our model, but its rate is suppressed relative to the invisible mode by \( \Gamma(n \to \chi \gamma) / \Gamma(n \to \chi A') \sim (\mu_n v')^2 \) where \( \mu_n \) is the
neutron magnetic moment and $v'$ is the VEV of the light scalar $\phi$ that breaks the U(1)$'$ symmetry. Since smaller values of $v'$ seem less likely in view of the hierarchy problem for scalar masses, the eventual detection of the visible decay mode could be expected. Dark neutron decay could also lead to effects in nuclear processes, with $^{11}$Be decays discussed as a particularly promising candidate for study in [58]. The dark matter could be discovered by direct detection, despite its small relic density. The UV completion of our model also requires heavy scalar quarks that could be accessible at LHC and detectable through their decays to first generation quarks or a jet plus missing energy.

**Note added.** After completion of this work, ref. [57] reported new limits on the decay channel $n \rightarrow \chi^+e^-$. Our model predicts such events from off-shell dark photon exchange, but at a very low rate. We computed the partial width for our benchmark models, finding $10^{-37} - 10^{-38}$ MeV, which is negligible. In addition, ref. [58] presented a new precise determination of the neutron axial vector coupling $g_A$ using lattice QCD. This value of the coupling is lower than the experimental average determined in [10], suggesting consistency between a dark decay contribution to the neutron lifetime and $g_A$.

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