$r$-PROCESS PRODUCTION SITES AS INFERRED FROM Eu ABUNDANCES IN DWARF GALAXIES

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ABSTRACT

Recent observations of $r$-process material in ultrafaint dwarf galaxies (UFDs) shed light on the sources of these elements. Strong upper limits on the Eu mass in some UFDs, combined with detections of much larger masses in a UFD, Reticulum II, and other dwarf galaxies, imply that Eu production is dominated by rare events, and that the minimal Eu mass observed in any UFD is approximately the amount of Eu mass produced per event. This is consistent with other independent observations in the Galaxy. We estimate, using a model-independent likelihood analysis, the rate and Eu (Fe) mass produced per $r$-process (Fe production) event in dwarf galaxies, including classical dwarfs and UFDs. The mass and rate of the Fe production events are consistent with the normal core-collapse supernova (CCSN) scenario. The Eu mass per event is $3 \times 10^{-3} M_\odot < m_{\text{Eu}} < 2 \times 10^{-4} M_\odot$, corresponding to a total $r$-process mass per event of $6 \times 10^{-3} M_\odot < m_{\text{r-process}} < 4 \times 10^{-2} M_\odot$. The rate of $r$-process events is $2.5 \times 10^{-4} < R_{\text{SN}}/M < 1.4 \times 10^{-3}$ as compared with the CCSN rate. These values are consistent with the total Eu mass observed in our own Galaxy, suggesting that the same mechanism is behind the production of $r$-process events in both dwarf galaxies and the Milky Way, and that it may be the dominant mechanism for production of $r$-process elements in the universe. The results are consistent with neutron star merger estimates but cannot rule out other rare core-collapse scenarios, provided that they produce significant amounts of $r$-process material per event.

Key words: galaxies: dwarf – stars: abundances – stars: neutron

1. INTRODUCTION

The origin of about half of the elements heavier than Fe, produced via the rapid neutron capture process ($r$-process), is still a mystery (Cowan et al. 1991; Wanajo & Ishimaru 2006; Arnould et al. 2007; Qian & Wasserburg 2007; see Thielemann et al. 2016 for a recent review). Core-collapse supernovae ($\text{CCSNe}$) have long been thought of as the production sites (Burbidge et al. 1957; Cameron 1957). This scenario requires either a neutrino-driven wind with high entropy (Woosley et al. 1994; Qian & Woosley 1996; Hoffman et al. 1997; Goriely et al. 2015), a highly magnetized outflow (Suzuki & Nagataki 2005; Metzger et al. 2008; Winteler et al. 2012; Vlasov et al. 2014; Møsta et al. 2015; Nishimura et al. 2015), wind from a black hole torus (Wanajo & Janka 2012), or fallback SNe (Fryer et al. 2006). It is unclear whether any one of those occurs frequently enough (Qian 2000). With this realization, the alternative scenario of compact binary mergers (neutron star–neutron star or neutron star–black hole binaries) that eject highly neutron-rich material in which $r$-process nucleosynthesis takes place (Lattimer & Schramm 1976; Symbalisty & Schramm 1982; Eichler et al. 1989; Freiburghaus et al. 1999) has been attracting more and more attention. Nucleosynthesis studies have shown that all $r$-process nuclides can be produced in the neutron star merger outflows (Wanajo et al. 2014; Wu et al. 2016). The discovery of macronova/kilonova candidates after short gamma-ray bursts (GRBs; Berger et al. 2013; Tanvir et al. 2013; Yang et al. 2015; Jin et al. 2016) has provided recent support to this idea.

Dwarf galaxies are composed of old stellar populations (e.g., Weisz et al. 2015). The chemical abundances of dwarf galaxies have been frozen since shortly after those galaxies formed. These chemical abundances have unique implications for the $r$-process production scenario (e.g., Tsujimoto & Shigeyama 2014). The $r$-process elements have been detected in classical dwarf galaxies (Shetrone et al. 2001, 2003; Venn et al. 2004; Letarte et al. 2010; Tsujimoto et al. 2015). In addition to stable $r$-process elements, thorium is found in a star of Ursa Minor, and its abundance ratio to stable $r$-process elements is lower than solar (Aoki et al. 2007), suggesting that events producing heavy $r$-process elements took place in this galaxy in the early universe $\sim$10 Gyr ago.

The Sloan Digital Sky Survey discovered several ultrafaint dwarf galaxies (UFDs; e.g., Willman et al. 2005; Belokurov et al. 2007). Remarkably, these UFDs contain only $\sim 10^3$–$10^5$ stars, and they are composed of an old and extremely metal-poor stellar population, suggesting that the UFDs are the closest objects to the first galaxies (see Bromm & Yoshida 2011 for a review). For some of them, the majority of the stars were likely to have formed before reionization, corresponding to a universe age of $\sim 13$ Gyr (Brown et al. 2014). Recently, Ji et al. (2016a) and Roederer et al. (2016) reported the first discovery of highly $r$-process-enriched stars in a UFD, Reticulum II, while there are only strong upper limits on the abundances of $r$-process elements for some other UFDs (Freyberg 2010, 2014; Roederer & Kirby 2014). These measurements that show large fluctuations in the $r$-process abundance imply that only a single $r$-process event took place in Reticulum II. Following these observations of $r$-process material in the classical dwarfs and UFDs, a question that naturally arises is what are the rate and amount of matter produced in $r$-process events that are consistent with these observations.

We estimate here the most likely mass ejection of Fe and Eu and rate of CCSNe per total luminosity and of $r$-process production events relative to CCSNe. We use a likelihood analysis, based on Poisson statistics. The formulation is independent of the specific nature of the sources of $r$-process
elements. We use the given measured Fe and Eu abundances in dwarf galaxies and their initial gas masses (to which those metals were injected). We assume that all dwarf galaxies (or alternatively, only UFDs) share the same mechanism for $r$-process production. The results in both cases (of all dwarf galaxies and just UFDs) strongly suggest that the $r$-process event rate is considerably smaller than the CCSN rate. They are comparable to the expectations from the neutron star merger scenario.

This paper is organized as follows. In Section 2 we describe the sample of UFD galaxies. A critical factor in the analysis is the initial gas masses in UFDs. We estimate the initial gas masses in UFDs in Section 3 using several different methods. We turn to the initial masses of Fe and $r$-process materials in Section 4. We apply a likelihood analysis in order to examine the Fe and $r$-process abundances in dwarf galaxies and estimate the rates and ejecta mass of CCSNe and $r$-process events needed in Section 5. We then compare the implied rate and $r$-process yields with those expected in the double neutron star (DNS) merger scenario in Section 6.1 and peculiar CCSNe in Section 6.2. Finally, we summarize our results in Section 7.

2. THE GALAXY SAMPLE

We consider dwarf spheroidal galaxies and focus in particular on UFDs that are composed of old and metal-poor stars (e.g., Simon & Geha 2007). We consider galaxies for which there are reported detections or upper limits on the Fe and Eu abundances. Our sample includes five UFDs: Reticulum II, Segue I, Segue II, Coma Berenices, and Ursa Major II. In addition, we consider six more massive classical dwarf galaxies: Carina, Sculptor, Draco, Leo I, Ursa Minor, and Fornax. We do not consider Sagitarius, since this galaxy has been shown to be considerably tidally disrupted (Ibata et al. 1995; Mateo et al. 1996; Majewski et al. 2003), and its mass is therefore very uncertain. Table 1 shows the $V$-band luminosities, $L_V$, the velocity dispersions, $\sigma$, and the half-light radii, $r_{1/2}$, taken from Walker et al. (2009, 2015), and the average Fe and Eu abundances (Shetrone et al. 2001, 2003; Frebel et al. 2010, 2014; Letarte et al. 2010; Roederer & Kirby 2014; Tsujimoto et al. 2015; Ji et al. 2016a, 2016b; Roederer et al. 2016). The errors of the average abundances shown in Table 1 include statistical and systematic uncertainties. If the systematic errors of the measurements for a galaxy are not available in the literature, we simply assume a systematic error of 0.2 dex.

3. THE CHEMICAL EVOLUTION OF DWARF GALAXIES

To evaluate the number of events that supplied Eu or Fe in each galaxy, the total amount of the elements produced in it is needed. We assume that the elemental abundances of stars in dwarf galaxies represent the amount of the elements in the gas from which the stars have been formed. The total amount of Fe and Eu produced in a galaxy during active star formation is estimated using the elemental abundances listed in Table 1, together with the gas mass into which metals are injected. The relatively low stellar luminosities as compared with the total halo masses suggest that UFDs have lost most of their initial gas due to either SN feedback or intergalactic medium reionization (Bovill & Ricotti 2009). Thus, the observed upper limits ($\lesssim 10^3 M_\odot$) on their current gas mass are not representative of the amount of material into which the $r$-process elements have been injected at the early stages of their evolution. Therefore, we estimate the amount of the gas based on the assumption that the initial gas mass is proportional to the halo mass within the size of the stellar spheroid.

When considering the mass loss from the dwarf galaxies, we assume that the gas is chemically homogeneous with the average abundances, as observed in the remaining stars. However, of course, the chemical mixing process in the gas is inhomogeneous, and a fraction of the produced material may escape from the galaxies, or alternatively, gas with a primordial composition may escape. Such effects should be taken into account when considering the abundance distribution of stars in each dwarf galaxy. These issues should be addressed with hydrodynamics simulations (see e.g., Pallottini et al. 2014; Hirai et al. 2015; Ritter et al. 2015) and are beyond the scope of this work.

The initial gas mass, $M_g$, should be between the total stellar mass of the system and 1/6 of the total halo mass of the system (we take here the typical fraction of 1/6 for the ratio of baryonic to total mass in a halo). As mentioned above, however, the stellar mass of UFDs is significantly smaller than the halo mass due to significant gas loss throughout the formation and evolution of the galaxy. We estimate $M_g$ using the halo mass within a given radius, $M_h(<r)$. This can be calculated directly from measurements of the half-light radius.
where the Plummer model for the stellar distribution with an isotropic and constant velocity dispersion is assumed. The halo masses within the half-light radius estimated with this formula by $M_h(<r_{1/2}) = 5r_{1/2}^2\sigma^2/2G$ are shown in Table 1. Of course, this formula can only be used up to the radius where the above assumptions are valid. As a fiducial model, we use $M_h \approx M_h(<r_{90})/6$, where $r_{90} \approx 3.71r_{1/2}$. According to the Plummer distribution, this choice corresponds to assuming that the material within the radius $r_{90}$, where 90% of the stellar mass is included, contributes to the chemical mixing of the injected metals. For comparison, we consider also initial halo masses that are smaller, $M_h(<r_{50})$, or larger than $M_h(<r_{90})$ by a factor of 3.

As the assumptions made in Equation (1) may be invalid at $r_{90}$ for some large dwarf galaxies, we also employ an alternative way to estimate the halo masses within $r_{90}$, using the Navarro–Frenk–White (NFW) mass profile with the model parameters derived in Walker et al. (2009), and integrating the distribution up to $r_{90}$. This method can only be carried out for the classical dwarfs. For the UFDs there are insufficient observations of stellar kinematics at large enough radii that would constrain the model parameters. In all but one case (Fornax), this estimate results in similar values to those obtained with the first method. Table 2 provides a summary of the different masses.

We compare the gas masses estimated here with those from the literature. Using a cosmological simulation of the first galaxies, Greif et al. (2010) show that Population II stars are formed from cold gas of $\sim 10^3 M_\odot$ at the center of a galaxy with a total mass of $\sim 10^6 M_\odot$. The smallest gas masses in our sample, $(2-3) \times 10^5 M_\odot$ for Reticulum II, Segue I, and Sugue II, are consistent with the result of Greif et al. (2010).

4. r-PROCESS ELEMENTS IN DWARF GALAXIES

The total masses of Fe and Eu produced in the system are estimated as

$$M_{\text{Fe}} \approx 120 \cdot 10^{[\text{Fe}/\text{H}]} M_\odot \left(\frac{M_g}{10^5 M_\odot}\right),$$

$$M_{\text{Eu}} \approx 3.7 \cdot 10^{-5+[\text{Eu}/\text{H}]} M_\odot \left(\frac{M_g}{10^5 M_\odot}\right),$$

where we assume that metals with an Eu (Fe) abundance of $[\text{Eu}/\text{H}]$ ([Fe/H]) are injected into a gas with an initial mass $M_g$ and used the solar abundances from Lodders (2003).

While only the abundances of Eu and some other r-process elements are measured, the total mass of r-process elements produced in a dwarf galaxy can be estimated by extrapolating the Eu abundance to other r-process ones using the solar r-process abundance pattern (Goriely 1999):

$$M_r \approx \begin{cases} 3.3 \cdot 10^{-2+[\text{Eu}/\text{H}]} M_\odot \left(\frac{M_g}{10^5 M_\odot}\right) & (A_{\text{min}} = 70) \\ 0.7 \cdot 10^{-2+[\text{Eu}/\text{H}]} M_\odot \left(\frac{M_g}{10^5 M_\odot}\right) & (A_{\text{min}} = 90) \\ 0.6 \cdot 10^{-2+[\text{Eu}/\text{H}]} M_\odot \left(\frac{M_g}{10^5 M_\odot}\right) & (A_{\text{min}} = 110) \end{cases}$$

where $A_{\text{min}}$ is the minimum mass number of r-process elements. It is worthwhile noting that the abundances of the r-process elements with atomic numbers of $Z < 40$, corresponding to $A < 90$, in Reticulum II are depleted compared to solar (Ji et al. 2016b) and similar to those of an extreme metal-poor star CS 22892–052 (Snedden et al. 2003). This suggests that there are two types of events, light and heavy r-process events, and only the latter took place in Reticulum II.

Figure 1 depicts the estimated total Fe and Eu masses for each dwarf galaxy as a function of the total stellar luminosity. Note that the Fe mass is proportional to the luminosity within uncertainties, implying that the number of SNe producing Fe is proportional to the number of stars. For the Eu masses, while a similar trend can be found, the dispersion is larger for the

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Table 2

Summary of Derived Quantities for the Dwarf Galaxies in the Sample

| Type          | Object          | $r_{90}$ (pc) | $M_h(<r_{90})$ ($10^6 M_\odot$) | $M_h(<r_{90})$ ($10^8 M_\odot$) |
|---------------|-----------------|---------------|---------------------------------|---------------------------------|
| UFDs          | Reticulum II    | 120±7         | 0.28±0.15                      |                                |
|               | Segue I         | 110±3         | 0.37±0.21                      |                                |
|               | Segue II        | 130±20        | 0.27±0.28                      |                                |
|               | Ursa Major II   | 520±90        | 4.2±1.8                        |                                |
|               | Coma Berenices  | 290±40        | 1.1±0.8                        |                                |
| Other dwarfs  | Draco           | 730±50        | 11±3                           | 9.8±1.5                        |
|               | Leo I           | 920±70        | 14±4                           | 13±4                           |
|               | Fornax          | 2500±100      | 61±10                          | 30±4                           |
|               | Carina          | 900±90        | 7.0±2.7                        | 5.3±1.5                        |
|               | Ursa Minor      | 1000±200      | 17±5                           | 14±6                           |
|               | Sculptor        | 970±150       | 15±4                           | 13±5                           |

Notes.

1. The initial gas mass estimated with the assumption of constant velocity dispersion up to $r_{90}$.
2. The initial gas mass estimated with the NFW model.

\[
\begin{align*}
M_h(r) & = \frac{5r_{1/2}^2\sigma^2(r/r_{1/2})^3}{G[1 + (r/r_{1/2})^2]} \\
& \approx 1.2 \times 10^3 M_\odot \left(\frac{r}{1 \text{ pc}}\right) \left(\frac{\sigma}{1 \text{ km s}^{-1}}\right)^2 \frac{(r/r_{1/2})^2}{1 + (r/r_{1/2})^2}, \\
\end{align*}
\]
We maximize, of course, this function over its free parameters. For the other UFDs there are strong upper limits, in some cases as small as $10^{-7} M_\odot$. This led Ji et al. (2016a) to suggest that there was only a single $r$-process production event in Reticulum II and none in the other UFDs.

5. THE $r$-PROCESS AND SN EVENT RATE AND AMOUNT OF MASS PRODUCED PER EVENT

5.1. The Statistical Method

We aim to constrain the event rate and mass per event for both SNe and $r$-process events. We begin with a description of the general statistical method that we use in both cases. We define the likelihood function in terms of two unknown parameters: $R$, the average rate of events, and $m_X$, the mass of an element $X$ produced by a single event.

Using Poisson statistics, we calculate the probability of obtaining $N$ events in the $i$th galaxy, given an expected number of events $N_{i,e}$. We assume that the mass of $X$ produced per event follows a normal distribution with an average of $\bar{m}_X$ and a standard deviation of $0.5\bar{m}_X$. For each $N$ the associated probability is then the Poisson probability of obtaining $N$ events times the probability that $N$ events would lead to an accumulated mass of element $X$ in the $i$th galaxy, $M_{X,i}$ (calculated from the observed values of [X/H] and $M_\odot$). Summing these probabilities over all $N$ values, we obtain the final probability: $P_i(M_{X,i}|R, \bar{m}_X)$. Finally, we write the likelihood function as

$$L(R, M_X) = \Pi_i P_i(M_{X,i}|R, \bar{m}_X).$$  

We maximize, of course, this function over its free parameters.

5.2. The SN Rate and Iron Production in Dwarf Galaxies

We begin by applying the method described in Section 5.1 to constrain the rate of Fe-producing SNe and the amount of Fe produced per event in these dwarf galaxies. The resulting likelihood function is seen in Figure 2. The main constraint is on the product of the two parameters. This reflects the fact that the average Fe mass per solar luminosity should match the observed ratio. The actual peak of the likelihood function is not strongly constrained, although interestingly, it coincides with an Fe mass per event of $\bar{m}_{Fe} = 0.1 M_\odot$ and a rate of $\approx 16$ SNe per $10^3 L_\odot$ (approximately $10^3$ stars).

These values are in fact expected from SN studies. In the local universe, two-thirds of CCSNe are Type II SNe that typically produce $0.02 M_\odot$ of Fe and Type Ibc SNe that produce $0.2 M_\odot$ (Drout et al. 2011; Kushnir 2015), and one-third of CCSNe are Type Ibc (Li et al. 2011). Therefore, the Fe production is dominated by SNe Ibc. In addition, since the star formation epoch in dwarf galaxies had lasted for a short timescale of $\sim 1$ Gyr, we assume that SNe Ia do not contribute to the Fe production. Thus, $0.1 M_\odot$ per CCSN is expected for dwarf galaxies. In addition, the rate of 16 SNe per $10^3 L_\odot$ is consistent with observations suggesting one SN per $100 M_\odot$ of star formation (e.g., Horiuchi et al. 2011; Li et al. 2011). The observational constraints on the rate and Fe mass per event
from the local universe are depicted by the red cross in Figure 2. This result suggests that the Fe production in each CCSN and their rate in metal-poor environments are similar to those in the local universe. In addition, it demonstrates the validity of this method.

5.3. Results and Implications for r-process Production in Dwarf Galaxies

We turn now to the production of Eu in r-process events. We calculate the rates relative to the CCSN rate, $R_{\text{rp/SN}}$. Using the results of the previous section (and independent analyses; see Section 5.2), we assume an average production of $0.1 \ M_\odot$ of Fe per CCSN. The average number of r-process events in the ith galaxy is then $N_{R,i} = R_{\text{rp/SN}} \times (M_{\text{Fe}}/0.1 \ M_\odot)$, where $M_{\text{Fe}}$ is the total amount of Fe in the same galaxy.

Figure 3 shows the results for two cases: all dwarf galaxies (left) and only UFDs (right). The likelihood function peaks at a rate relative to the SN rate of $R_{\text{rp/SN}} = 6 \times 10^{-4}$ ($R_{\text{rp/SN}} = 3 \times 10^{-4}$), and at a mass per event of $\tilde{m}_{\text{Eu}} = 9 \times 10^{-5} \ M_\odot$ ($\tilde{m}_{\text{Eu}} = 7 \times 10^{-6} \ M_\odot$), corresponding to a total mass of r-process matter produced per event of roughly $1.7 \times 10^{-2} \ M_\odot$ ($1.3 \times 10^{-3} \ M_\odot$). The strong upper limits on the Eu abundance of some galaxies, coupled with the detection of a significant amount of Eu in galaxies of similar masses, imply that the Eu mass produced per event should be approximately the smallest amount detected in any given galaxy. Notice that this situation is very different than the case for Fe production, where the same statistical method results in no preference for a small number of events per galaxy. This leads to a relative rate of r-process to CCSN events $\ll 1$. Thus, we can rule out the possibility that normal CCSNe dominate the production of r-process materials in dwarf spheroidal galaxies.

Interestingly, this rate of Eu production is consistent with the constraints from our own, much more massive Galaxy. Assuming one CCSN per 100 $M_\odot$ of star formation, and given a total stellar mass of $6.4 \times 10^{10} \ M_\odot$ (McMillan 2011), we obtain $6.4 \times 10^8$ such SNe in the history of the Milky Way (Venn et al. 2004). Combining this with a total Eu mass of $\approx 18 \ M_\odot$ leads to $R_{\text{rp/SN}} = 2.8 \times 10^{-3} (\tilde{m}_{\text{Eu}}/10^{-3} \ M_\odot)^{-1}$, with a systematic uncertainty of a factor of $\sim 3$. The range permitted by these observations is depicted as the area between the dashed lines in Figure 3. As seen in that figure, this range is consistent with the best-fit parameters found for the dwarf galaxies. Furthermore, the low rate is consistent with $R_{\text{rp/SN}} < 5 \times 10^{-3}$, which Hotokezaka et al. (2015) find in order to reproduce the $^{24}$Pu abundances of both the early solar system material (Turner et al. 2007) and the present-day deep-sea archives (Wallner et al. 2015). These suggest that the r-process production in the Milky Way is dominated by the same events as in dwarf galaxies. Therefore, these results for the rate and mass per event can be generalized, and the same process could be the dominant source of r-process production in the whole universe.

5.4. The Robustness of the Method and Dependence on Parameters

We turn now to exploring the dependence of the results on the assumed halo masses. As mentioned in Section 3, there is some uncertainty in the values of these masses. We repeat the calculation (for all dwarf galaxies) with halo masses of $M_h(<r_{50})$ (smaller by about an order of magnitude as compared with $M_h(<r_{90})$) and $3M_h(<r_{90})$. For $M_h(<r_{50})$ ($3M_h(<r_{90})$), the likelihood peaks at an Eu mass per event of $\tilde{m}_{\text{Eu}} = 3 \times 10^{-3} \ M_\odot$ ($\tilde{m}_{\text{Eu}} = 2.5 \times 10^{-4} \ M_\odot$) and at a rate relative to the SN rate of $R_{\text{rp/SN}} = 2 \times 10^{-3}$ ($R_{\text{rp/SN}} = 3 \times 10^{-4}$). As expected, the amount of Eu mass per event is approximately the minimal Eu mass observed in any galaxy and thus tracks linearly the halo mass. In addition, since $R_{\text{rp/SN}}$ is roughly

$$R_{\text{rp/SN}} = \frac{M_{\text{Eu}}\tilde{m}_{\text{Fe}}}{M_{\text{Fe}}\tilde{m}_{\text{Eu}}},$$

and since $M_{\text{Eu}}$, $M_{\text{Fe}}$, $\tilde{m}_{\text{Eu}}$ are linear in the halo mass, it follows that $R_{\text{rp/SN}}$ is inversely proportional to this quantity. Most
importantly, the conclusion that $R_{\text{GRB}} < 1$ holds in all of these cases.

6. IMPLICATIONS FOR THE SCENARIOS OF $r$-PROCESS PRODUCTION

6.1. DNS Mergers

The $r$-process mass per event that we find in the likelihood analysis described in Section 5 is roughly consistent with expectations for DNS mergers from simulations. These simulations typically find ejecta masses of $10^{-3} - 10^{-2} M_\odot$, corresponding to Eu masses of $5 \times 10^{-6} - 5 \times 10^{-5} M_\odot$ (Korobkin et al. 2012; Bauswein et al. 2013; Perego et al. 2014; Just et al. 2015; Sekiguchi et al. 2015; Radice et al. 2016; Wu et al. 2016). The results are also consistent with macronova estimates (Berger et al. 2013; Hotokezaka et al. 2013; Piran et al. 2014; Jin et al. 2016).

The strong upper limits of $\lesssim 10^{-6} M_\odot$ for the other UFDs imply that such events did not take place in these UFDs. We turn now to estimating the expected rates of DNS mergers in these galaxies and comparing them to the results from the likelihood analysis in Section 5. The expected number of $r$-process production events by DNS inside a UFD during its star formation epoch is

$$R_{\text{DNS}} = f (v_{\text{CM}} < v_{\text{esc}}, t_{\text{m}} < t_{\text{SF}}) \frac{\text{Number of mergers}}{\text{Number of ccSNe}},$$

where $f (v_{\text{CM}} < v_{\text{esc}}, t_{\text{m}} < t_{\text{SF}})$ is the fraction of mergers with a center-of-mass velocity, $v_{\text{CM}}$, smaller than the escape velocity of a UFD, $v_{\text{esc}}$, and with a merger time, $t_{\text{m}}$, shorter than the duration of the star formation phase, $t_{\text{SF}}$. The small escape velocities from UFDs (down to $\approx 15$ km s$^{-1}$ in some cases) and the relatively short durations of their star formation, $\lesssim 1$ Gyr, reduce the number of mergers providing $r$-process elements in the star-forming gas. However, in Beniamini et al. (2016) we have shown that since many DNS systems receive small kicks at birth (Beniamini & Piran 2016), a large fraction of them would have $v_{\text{CM}} < 15$ km s$^{-1}$. Furthermore, given limits on the separation of the double pulsar system before its second collapse, a significant fraction of systems are expected to both remain confined in UFDs and merge within less than a gigayear. All together, we estimate that

$$6 \times 10^{-2} \lesssim f (v_{\text{CM}} < v_{\text{esc}}, t_{\text{m}} < t_{\text{SF}}) \lesssim 0.6.$$ 

Therefore, using our result in Section 5, the number of mergers per CCSN is estimated as $5 \times 10^{-4}$ to $2 \times 10^{-2}$.

We compare the results also with the merger rate estimated using short GRB observations. The local short GRB rate is estimated as $4.1^{+2.1}_{-1.0} f_b^{-1}$ Gpc$^{-3}$ yr$^{-1}$ (Wanderman & Piran 2015), where $f_b^{-1}$ is a beaming factor that is in the range $1 < f_b^{-1} < 100$ (Fong et al. 2015). The rate of local CCSNe is $7.1^{+1.4}_{-1.4} \times 10^5$ Gpc$^{-3}$ yr$^{-1}$. Therefore, the number of short GRBs per CCSN is $5.8^{+1.2}_{-0.8} \times 10^{-5} f_b^{-1}$, consistent with our estimates above.

6.2. Peculiar CCSNe

The low rate and large amount of $r$-process elements per event $\sim 0.01 M_\odot$ challenge the standard CCSN scenarios. A neutrino-driven wind of proto-neutron stars of normal CCSNe is clearly incompatible with the low rate. However, the low rate can be consistent with a peculiar astrophysical explosion associated with a core collapse of massive stars. For instance, a magnetically powered outflow from newly born magnetars has been proposed as the site of the $r$-process nucleosynthesis (Suzuki & Nagataki 2005; Metzger et al. 2008; Winteler et al. 2012; Vlasov et al. 2014; Móst 2015; Nishimura et al. 2015). This could happen in a peculiar SN (e.g., Winteler et al. 2012) or in a long GRB, in which case the magnetic outflow also powers the GRBs themselves. A neutrino-driven wind from an accretion torus of newly formed black holes (Wanajo & Janka 2012) and fallback SNe (Fryer et al. 2006) have also been suggested as the production sites.

The rate of long GRBs has been estimated as $1.3^{+0.4}_{-0.2} \times 10^{-2}$ Gpc$^{-3}$ yr$^{-1}$ before beaming corrections (Wanderman & Piran 2010). This is comparable, up to a factor of 3, with the rate of short GRBs. Given a lower rate, more $r$-process mass per event is required. But, of course, this also depends on an unknown beaming factor. Low-luminosity GRBs and superluminous SNe have also been proposed to involve magnetized outflows (or for the latter, winds from accretion tori around black holes). The rates of these events are $230^{+450}_{-190}$ Gpc$^{-3}$ yr$^{-1}$ (Soderberg et al. 2006) and $91^{+76}_{-36}$ Gpc$^{-3}$ yr$^{-1}$ (Praj et al. 2016), corresponding to a rate relative to CCSNe of approximately $10^{-3} - 10^{-2}$.

This is at the upper end of the permitted range that we find (Section 5) and would, in turn, require the $r$-process mass per event to be at the low end of the permitted range ($\approx 6 \times 10^{-3} M_\odot$).

Wanajo & Janka (2012) have estimated that a neutrino-driven wind from a black hole accretion torus can produce $\sim 10^{-3} M_\odot$, which seems too small to be consistent with the permitted range that we find here.$^3$ Other estimates of $r$-process material production yield $\approx 0.01 M_\odot$ for an SN magnetized driven jet (Nishimura et al. 2015) and $\lesssim 0.01 M_\odot$ for a magnetized neutrino-driven wind (Vlasov et al. 2014). Since these processes require rapid rotation, and hence low metallicity, these authors estimate that the rate of such events is low compared to regular SNe. However, the exact rates are uncertain.

7. CONCLUSIONS AND DISCUSSIONS

We have explored the question of iron and $r$-process production in dwarf spheroidal galaxies in a model-independent fashion. We assume that all dwarf galaxies (or alternatively, only UFDs) share the same mechanism for production of these elements. We then use the element abundances and apply a likelihood method to estimate the most likely rates and element mass produced per such event. Using the mass within the radius that contains 90% of the galaxies’ light, $M_{\text{g}}(< r_{\text{eff}})$, as a proxy for the halo masses (which in turn provides the initial gas mass), we find that on average $0.1 M_\odot$ of Fe is produced per CCSN and that the rate is approximately 16 CCSNe per $10^4 L_\odot$, verifying the estimated values of these parameters from independent studies using different methods (Horiiuchi et al. 2011).

Turning now to $r$-process events, we find that the Eu mass per event is between $3 \times 10^{-5} M_\odot < M_{\text{Eu}} < 2 \times 10^{-4} M_\odot$ and $2.5 \times 10^{-6} M_\odot < M_{\text{Eu}} < 3.5 \times 10^{-5} M_\odot$ for UFDs only. The very strong upper limits on the Eu mass in some galaxies, combined with detections of significantly larger masses in other

$^3$ The amount of the torus wind depends on the black hole spin (Fernández et al. 2015; Just et al. 2015). There may be parameter regions where more massive winds can be produced.
dwarfs, imply that Eu production is dominated by rare events and that the minimal Eu mass observed in any galaxy is approximately the amount of Eu mass produced per event. This corresponds to a total $r$-process mass of $6 \times 10^{-3} M_{\odot} < m_{r \text{-process}} < 4 \times 10^{-2} M_{\odot}$ ($5 \times 10^{-4} M_{\odot} < m_{r \text{-process}} < 7 \times 10^{-3} M_{\odot}$ for UFDs only), assuming that $r$-process events dominate the production of elements with mass number $A > 90$. The rate of these events is $2.5 \times 10^{-4} < R_{\text{rp}/SN} < 1.4 \times 10^{-3}$ as compared with the CCSN rate ($1.6 \times 10^{-5} < R_{\text{rp}/SN} < 1.4 \times 10^{-3}$ for UFDs only). We conclusively rule out the possibility that the rates of $r$-process events could be comparable to that of CCSNe. Interestingly, both the $r$-process mass per event and the rate are, however, consistent with expectations for DNS mergers. However, rare magnetic-driven SNe, long GRBs, superluminous SNe, or even low-luminosity GRBs are all possible candidates. Furthermore, these values are consistent with the total Eu mass observed in our own Galaxy. This suggests that the same mechanism is behind the production of $r$-process events in both UFDs and the Milky Way, and that it may be the dominant mechanism for production of $r$-process elements as a whole in the universe. Association of a gravitational-wave event from a DNS merger and a clear macronova from which the amount of $r$-process production can be well estimated could therefore confirm or reject this scenario.

A large scatter in the abundances of $r$-process elements is also seen in metal-poor stars in our own Galaxy, which again supports rare events (e.g., Cescutti & Chiappini 2014; Tsujimoto & Shigeyama 2014; Wehmeyer et al. 2015). In addition, Hotokezaka et al. (2015) have shown that the rarity of $r$-process events is broadly consistent with $^{244}$Pu abundances of both the early solar system material (Turner et al. 2007) and the present-day deep-sea archives (Wallner et al. 2015), which is difficult to explain otherwise. The $r$-process element enrichment in halo stars with very low metallicities, proposed as a problem for this scenario (Argast et al. 2004), can be resolved by taking into account the turbulent mixing of material in the galaxy (Piran et al. 2014), the assembly of subhalos during the formation of the Galaxy (Komiya et al. 2014; Ishimaru et al. 2015; Shen et al. 2015; van de Voort et al. 2015), the large typical distances between the locations of the stellar collapses and the eventual mergers (Beniamini et al. 2016), and the likely possibilities of rapid mergers and stellar collapses with small amounts of mass ejecta (Beniamini & Piran 2016; Beniamini et al. 2016).

Given the orbits of the observed DNS systems in the Galaxy, a significant amount of DNS systems are expected to both remain confined within UFDs and merge within a relatively short time since formation (Beniamini et al. 2016). Using these results and assuming that $r$-process production is dominated by DNS mergers, we estimate the DNS merger rate to be $5 \times 10^{-4}$ to $2 \times 10^{-3}$ per CCSN. This is comparable to the rates estimated using other methods such as from short GRBs or from population synthesis.

There are two major differences between the DNS and core-collapse scenarios. First, DNS mergers have delay times relative to the star formation, but the core-collapse events do not. Moreover, since the rare core-collapse events, discussed above, may take place preferably in low-metallicity environments, they may even precede the average star formation and produce $r$-process elements in very low metallicity environments. However, the region will be “polluted” by mass outflow from the progenitor stars, oxygen and carbon from winds, and Fe from the associated SN. Second, during the formation of the second neutron star in a DNS, the center of mass receives a velocity of $\sim 15$ km s$^{-1}$ (Beniamini et al. 2016). This is slower than the typical escape velocity from UFDs but fast enough to run away from the star-forming regions where they have been formed. Thus, the mergers can take place in low-metallicity environments that are “unpolluted” by the progenitors. This depends, of course, on the pace of turbulent mixing within the UFD. These differences should be reflected in the distribution of Eu and Fe within the galaxies and in the chemical history of the Galaxy. Abundance measurements for a larger number of stars in Reticulum 2 and other dwarf galaxies may provide vital information that may enable us to distinguish between the two scenarios.

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