Second-order correlations in an exciton-polariton Rabi oscillator

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We develop the theoretical formalism to calculate second-order correlations in dissipative exciton-polariton system and we propose intensity-intensity correlation experiments to reveal the physics of exciton-light coupling in semiconductor microcavities in the Rabi oscillation regime. We predict a counter-intuitive behaviour of the correlator between upper and lower polariton branches: due to the decoherence caused by stochastic exciton-photon conversions this correlator is expected to decrease below 1, while the individual second-order coherence of upper and lower polaritons exhibits non-monotonous bunching.

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Introduction.—Recent decades are manifested by a tremendous progress in the physics of strongly-coupled light-matter systems. In particular, semiconductor microcavity [1] structures have demonstrated a number of fascinating coherent many-body effects, e.g., polariton lasing [2] and formation of Bose-Einstein condensates of exciton-polaritons [3]. Exciton-polaritons may be viewed as quantum superposition states of light and matter [4]. Their dual nature is visualised in polariton Rabi oscillations: beats between exciton and photon states in semiconductor microcavities in the strong coupling regime [5]. Usually, the Rabi oscillations are excited by a short laser pulse which simultaneously and equally populates the upper polariton (UP) and the lower polariton (LP) branches. Initially, the system is in a purely photonic state. Then, due to the splitting between UP and LP branches, it starts developing the excitonic component, becomes purely excitonic after several fractions of a picosecond, then returns to the photonic state, and so on. Polariton Rabi-oscillations have been experimentally observed by many groups [6–8]. Usually, only several periods of oscillations could be resolved in these studies. The magnitude of oscillations was found to decrease with time and eventually vanish due to some decoherence processes. The nature of these processes still needs to be revealed. One process is the phonon-assisted scattering between UP and LP branches that leads to depopulation of the upper branch and breaks coherence between two branches [9]. In the recent work [10] we have addressed a process of stochastic exciton-photon conversion, which is crucial in the weak exciton-photon coupling regime and possibly plays an important role in the strong coupling regime too. The question of existence of stochastic processes even in the strong coupling regime is important for understanding the quantum properties of exciton-polaritons. In which extent polaritons can be considered as coherent superpositions of photons and excitons? How accurate would be the description of a polariton gas in terms of an exciton-photon mixture? The dynamics of exciton-photon correlators in the polariton lasing regime calculated in our previous paper [10] would help answering these questions. Unfortunately, direct experimental measurements of exciton-photon correlations seem quite tricky. Here we show that instead of counting individual excitons and photons one can access the stochastic exciton-photon transformation kinetics by doing a purely optical and much simpler experiment. Namely, one can study two-color intensity-intensity correlations of light emitted from UP and LP branches in the strong coupling regime. The scheme of proposed optical experiment is shown in Fig. 1.

The finite lifetime of excitons and photons does not destroy the coherence of Rabi oscillations, only the amplitude of the signal decays in time after pulsed excitation of the system. The stochastic conversion of particles, however, has a profound destructing effect on the Rabi process. The result is qualitatively similar to the suppression of the tunneling for a particle in a double-well potential in the presence of dissipation [11]. In this Letter, we present the exact theory of second-order correlations on exciton-polariton system in the presence of dissipation due to exciton-photon conversion. We predict a counterintuitive variation of the intensity-intensity correlator between UP and LP branches (two-color correlation experiment) and show that this variation may be considered as a signature of stochastic conversions in the strong coupling regime.

From the point of view of quantum statistics, the loss of coherence in a light source is manifested by the variation of the intensity-intensity correlator $g^{(2)}$ that ranges between 1 (purely coherent light) and 2 (thermal distribution of photons) for classical sources [12]. In the regime of polariton Rabi oscillations, the quantum coherence between two branches can be characterised by a sim-
The dissipative exciton-polariton system can be described by the Liouville equation for the full density matrix \[ \frac{d\hat{\rho}(t)}{dt} = \frac{i}{\hbar} [\hat{\rho}, \hat{H}_0] - \sum_j g_j \left( [\hat{A}_j, \hat{\rho}] + [\hat{\rho}, \hat{A}_j] \right). \] (1) We introduced three \((j = x, c, u)\) single-particle Lindblad terms with \(\hat{A}_x = \hat{a}, \hat{A}_c = \hat{b}, \text{ and } \hat{A}_u = (\hat{a} + \hat{b})\). The first two terms describe the direct depopulation of the exciton and photon states. The third term with coefficient \(g_u \equiv \gamma^c\) simply renormalizes the exciton and the cavity photon lifetimes, \(\tau_x = (g_x + \gamma^x)^{-1}\) and \(\tau_c = (g_c + \gamma^c)^{-1}\), on the one hand. On the other hand, it models the cross-relaxation and allows phenomenologically for an additional decay from the upper polariton state that is crucial for description of realistic microcavities. Finally, there are two \((j = xc, cx)\) terms describing the conversion processes, with \(\tau_{xc} = \tau_{cx} = g_{xc}^{-1}\) being the exciton-photon conversion time and operators \(\hat{A}_{xc} = \hat{b}^\dagger \hat{a}\) and \(\hat{A}_{cx} = \hat{a}^\dagger \hat{b}\).

In what follows we shall consider different first- and second-order correlations. For the density matrix satisfying (1) it is possible to find the closed systems of equations for the correlators of any order. To proceed, it is convenient to introduce the spin operators \(\hat{s}_\mu\) with \(\mu = 0, 1, 2, 3\):

\[
\begin{align*}
\hat{s}_0 &= \frac{1}{2} (\hat{a}^\dagger \hat{a} + \hat{b}^\dagger \hat{b}), \\
\hat{s}_1 &= \frac{i}{2} (\hat{a}^\dagger \hat{a} - \hat{b}^\dagger \hat{b}), \\
\hat{s}_2 &= \frac{i}{2} (\hat{a}^\dagger \hat{b} - \hat{b}^\dagger \hat{a}), \\
\hat{s}_3 &= \frac{1}{2} (\hat{a}^\dagger \hat{b} + \hat{b}^\dagger \hat{a}).
\end{align*}
\]

The intensities of light emitted from UP and LP branches can be found from averages \(S_{\mu}(t) = \langle \hat{s}_\mu \rangle\), which satisfy

\[
\begin{align*}
\dot{S}_0 &= -\Gamma S_0 + \gamma S_1 - \gamma^c S_3, \\
\dot{S}_1 &= -\Gamma S_1 - \Gamma S_3, \\
\dot{S}_2 &= -\Gamma S_2 + \Delta S_3 + \omega_R S_1, \\
\dot{S}_3 &= -\Gamma S_3 + \gamma^c S_0 - \Delta S_0 - \Delta S_2.
\end{align*}
\]

Here \(\Gamma = (g_x + g_c + 2\gamma^c)/2\) and \(\gamma = (g_x - g_c)/2\).

To compute the second-order coherence it is convenient to operate with the averages of the normal ordered products \(S_{\mu\nu}(t) = \langle \hat{s}_\mu \hat{s}_\nu \rangle\), with \(\mu, \nu = 0, 1, 2, 3\). The components of the symmetric tensor \(S_{\mu\nu}(t)\) obey the equations
Here we omitted the equation for $S_{00}$, which follows from the identity $S_{00} = S_{11} + S_{22} + S_{33}$, namely, $S_{00} = -2\tau S_{00} + 2\tau S_{01} - 2\tau S_{03}$. It should be noted that the Eqs. (4a-d) and (5a-i) are exact consequences of the quantum Liouville equation for the density matrix (1). No quasi-classical assumptions have been made, and one can use these equations for the analysis of evolution of the quantum states of the Rabi oscillator.

In what follows, we consider the pulsed excitation of a photonic state assuming that an ultrashort pulse of light arrives at $t = 0$. For the case of initial coherent photonic state with $N$ photons in average, the initial condition to Eqs. (4a-d) are $S_{0}(0) = -S_{1}(0) = N/2$ and $S_{2}(0) = S_{3}(0) = 0$. For Eqs. (5a-i) we have $S_{00} = S_{11} = -S_{01} = N^{2}/4$, and the other components of the tensor are zero. In the exotic reference case of an initial Fock state with $N$ photons, the latter should be changed to $S_{00} = S_{11} = -S_{01} = N(N-1)/4$.

In the most experimentally relevant case of photonic excitation the components $S_{0,1,2}(t)$ exhibit decaying Rabi oscillations, and in the absence of stochastic processes ($\tau_{xc}^{-1} = 0$) one has $S_{0}^{2} = S_{1}^{2} + S_{2}^{2} + S_{3}^{2}$. This equality is violated in the case of a finite stochastic conversion time $\tau_{xc}$, since the exciton-photon conversion results in decoherence. The evolution of tensor $S_{\mu\nu}$ is more complex and it is characterized by appearance of finite off-diagonal correlations at long times. Even in the simplest case of $\gamma' = 0$ and zero detuning, which is shown in Fig. 2, there are six non-zero components. If exciton and photon decay rates are slow compared to the decoherence rate ($\tau_{c}, \tau_{c} \gg \tau_{xc}$), the diagonal $S_{11}, S_{22}$, and $S_{33}$ components tend to $S_{00}/3$ at long times, indicating the equidistribution of populations of excitons and photons. This tendency is only approximately observed if decay and decoherence rates are of the same order. For the parameters in Fig. 2, we have at long times $S_{11} \rightarrow 0.331 S_{00}$, $S_{22} \rightarrow 0.342 S_{00}$, and $S_{33} \rightarrow 0.327 S_{00}$. Also, at long times, there appear finite off-diagonal correlations, $S_{01} \rightarrow 0.0124 S_{00}$, $S_{02} \rightarrow 0.1225 S_{00}$, and $S_{12} \rightarrow 0.00147 S_{00}$.

Intensity-intensity correlations.—The Hamiltonian (2) is diagonalized in the basis of LP and UP states with the annihilation operators $\hat{c}_{i} = \hat{a} \cos \phi - \hat{b} \sin \phi$ and $\hat{c}_{u} = \hat{a} \sin \phi + \hat{b} \cos \phi$, where the auxiliary angle $\phi$ is defined by $\tan(2\phi) = \omega R/\Delta$. The polariton occupation numbers are

$$n_{i} = \langle \hat{c}_{i}^{\dagger} \hat{c}_{i} \rangle = S_{0} \mp S_{1} \cos(2\phi) \pm S_{3} \sin(2\phi),$$

where the upper and the lower signs correspond to the UP ($i = u$) and the LP ($i = l$) branches, respectively.
There are several second-order correlators that can be experimentally accessed for an exciton-polariton Rabi oscillator. Those of major interest are the UP-LP intensities correlator $g_{ul}(t)$, which can be determined as

$$
g_{ul} = \frac{\langle \hat{c}^\dagger_l \hat{c}^\dagger_u \hat{c}_u \hat{c}_l \rangle}{\langle \hat{c}^\dagger_u \hat{c}_u \rangle \langle \hat{c}^\dagger_u \hat{c}_u \rangle},$$

$$= \frac{S_{11} \sin^2(2\phi) + S_{22} + S_{33} \cos^2(2\phi) + S_{13} \sin(4\phi)}{S_0^2 - |S_1 \cos(2\phi) - S_3 \sin(2\phi)|^2},$$

(7)

the second-order coherence for UP and LP,

$$g_i^{(2)} = n_i^{-2} \langle \hat{c}^\dagger_i \hat{c}^\dagger_i \hat{c}_i \hat{c}_i \rangle$$

$$= n_i^{-2} \left[ S_{00} + S_{11} \cos^2(2\phi) + S_{33} \sin^2(2\phi) \pm 2S_{03} \cos(2\phi) \cos(4\phi) - S_{13} \sin(4\phi) \right],$$

(8)

with the same convention about the signs as in Eq. (7), and the generalized UP-LP correlator expressed trough the previous three correlators,

$$G_{ul} = \frac{g_{ul}^2}{g_u^2 g_l^2} = \frac{\langle \hat{c}^\dagger_l \hat{c}^\dagger_u \hat{c}_u \hat{c}_l \rangle^2}{\langle \hat{c}^\dagger_u \hat{c}_u \rangle \langle \hat{c}^\dagger_u \hat{c}_u \rangle}.$$ 

(9)

The above correlators equate to unity for coherent Rabi oscillations, and their deviation from 1 is a smoking gun of the stochastic exciton-photon conversion processes. Moreover, the effect of decoherence is well pronounced even for rather long conversion times $\tau_{xc}$, as it is seen in Fig. 3(a-c). The UP-LP correlator (7) shown in Fig. 3(a) decreases below 1, and for short enough $\tau_{xc}$ can become close to 2/3. This happens because the exciton-photon conversion process tend to form the equidistribution of particles, and the perfect equidistribution gives $g_{ul} = 2/3$ [10]. However, the equidistribution does not hold with time, because the excitons and photons are removed from the cavity with different rates $\tau_x^{-1} \neq \tau_c^{-1}$. As a result, the time dependence of $g_{ul}$ is nonmonotonous and there is a slow growth of this correlator at long times. The evolution of the polariton second-order coherence (8) is also in general nonmonotonous and exhibits bunching, $g_i^{(2)} > 1$, see Fig. 3(b). Since both $g_{ul}$ and $g_i^{(2)}$ increase at long times, it is convenient to consider the combined correlator $G_{ul}$ (9) which tends to a constant value at $t \to \infty$. This saturation value is 1/4 for short $\tau_{xc}$ [10]. When $\tau_{xc}$ is comparable or larger than $\tau_c$ the saturation value is bigger than 1/4 and it depends on $\Delta$ and $\gamma$. All correlators shown in Fig. 3(a-c) reflect the presence of Rabi oscillations in the system.

In conclusion, two-color intensity-intensity correlation measurements between UP and LP branches in the regime of Rabi-oscillations are expected to shed light onto decoherence caused by stochastic exciton-photon conversion processes in the system. The two-color correlator is predicted to go below 1 if the stochastic processes are important. This prediction allows for a relatively simple experimental test of the decoherence of polariton Rabi oscillator and verification of the quantum superposition nature of an exciton-polariton state in the strong coupling regime. Finally, we note that a straightforward extension of our formalism permits evaluation of the noise spectra of UP and LP emission intensities. These spectra are also expected to be sensitive to the stochastic exciton-photon conversion.

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