Quasar Accretion Disk Sizes from Continuum Reverberation Mapping from the Dark Energy Survey

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Abstract

We present accretion disk size measurements for 15 luminous quasars at $0.7 \leq z \leq 1.9$ derived from griz light curves from the Dark Energy Survey. We measure the disk sizes with continuum reverberation mapping using two methods, both of which are derived from the expectation that accretion disks have a radial temperature gradient and the continuum emission at a given radius is well described by a single blackbody. In the first method we measure the relative lags between the multiband light curves, which provides the relative time lag between shorter and longer wavelength variations. From this, we are only able to constrain upper limits on disk sizes, as many are consistent with no lag the 2σ level. The second method fits the model parameters for the canonical thin disk directly rather than solving for the individual time lags between the light curves. Our measurements demonstrate good agreement with the sizes predicted by this model for accretion rates between 0.3 and 1 times the Eddington rate. Given our large uncertainties, our measurements are also consistent with disk size measurements from gravitational microlensing studies of strongly lensed quasars, as well as other photometric reverberation mapping results, that find disk sizes that are a factor of a few (~3) larger than predictions.

Key words: accretion, accretion disks – galaxies: active – quasars: general

Supporting material: figure set, machine-readable table

1. Introduction

The spectra of quasars and less-luminous active galactic nuclei (AGNs) are characterized by the presence of both narrow emission lines that originate far from the central engine and broad ones that originate close to the supermassive black hole (SMBH). These lines are superposed on a continuum mostly due to thermal radiation from the accretion disk that peaks in the ultraviolet. Understanding the size and structure of this accretion disk is important because it is energetically dominant, drives most of the other emission, and probes the growth of the central SMBH.

The canonical quasar accretion disk model is the optically thick, geometrically thin disk (Lynden-Bell 1969; Shakura & Sunyaev 1973). The disk emission is a combination of the local thermal emission of the viscously dissipated energy and reprocessing of emission from the inner regions. Thin disks are stable at low to moderate accretion rates compared to the Eddington rate. There are also stable slim accretion disks (Abramowicz et al. 1988; Narayan & Yi 1995), where the optically thin disks are no longer geometrically thin and the accretion rates are near or super-Eddington. Hall et al. (2018) propose an extension to the thin-disk model for the accretion where the emission is modified by a low-density disk atmosphere to be non-thermal, making disks appear to be larger than would be inferred from a blackbody.

Viscously heated material moving through the accretion disk at radii larger than the innermost stable circular orbit emits photons as

$$\sigma T^4 = \frac{3GMm_\odot}{8\pi R^3},$$

where $T$ is the temperature of the material, $M$ is the mass of black hole, $m_\odot$ is the accretion rate onto the black hole, and $R$ is the orbital radius of the material (Collier et al. 1998). The size, $R$, of this standard thin disk at an effective emitting wavelength $\lambda_0$, defined by the region where the disk temperature is $kT = hc/\lambda_0$, and assuming the annulus is emitting as a blackbody (Collier et al. 1998; Morgan et al. 2010), can be rewritten as

$$R_{\lambda_0} = \left[\frac{45G\lambda_0^4 m_\odot(3 + \kappa)}{16\pi^3hc^2}\right]^{1/3}$$

$$= 9.7 \times 10^3 \left(\frac{\lambda_0}{\mu m}\right)^{1/3} \left(\frac{M}{10^9 M_\odot}\right)^{2/3} \left(\frac{L}{\eta L_\odot}\right)^{1/3} \text{ cm},$$

where $M$ is again the black hole mass, $\dot{m}$ is the accretion rate, $\kappa$ is the ratio of external to local radiative heating, $L_\odot$ is the Eddington luminosity, and $\beta$ is the power-law index on $\lambda$, which would be $4/3$ from Equation (2). We introduce this $\beta$ here as we will use it throughout the paper. The above scaling relationship assumes that $\kappa = 0$. The accretion rate can be related to the luminosity by $L = \eta\dot{m} c^2$, where $\eta$ is the radiative efficiency of converting the accreted mass into energy. From Equation (2), we find that the accretion disk size should scale as $\lambda^{4/3}$. Given the blackbody emission assumption that $kT = hc/\lambda_0$, this predicts that the temperature also goes as $T \propto R_{\lambda_0}^{-1/3} \propto R_0^{3/4}$. We generalize the disk radius at an emitting wavelength $\lambda$ as

$$R_{\lambda} = R_{\lambda_0}\left(\frac{\lambda}{\lambda_0}\right)^{\beta/3},$$

where the standard thin disk has $R_{\lambda_0}$ as given in Equation (2) and $\beta = 4/3$ is the prediction for infalling viscously heated material.

If the temporal variability of the disk is driven by fluctuations in the irradiated flux from a central source, such as in the “lamppost” model (see Cackett et al. 2007 and references therein), then the time delay for light to reach any radius in the disk implies that there should be delays in the response at different wavelengths. If the size–wavelength relation is given by Equation (3), then the lag $\tau$ between emission from different annuli in the disk with effective emitting wavelengths $\lambda_0$ and $\lambda$ should be of the form

$$\tau = \frac{R_{\lambda_0}}{c} \left[\left(\frac{\lambda}{\lambda_0}\right)^{\beta/3} - 1\right].$$

The above derivations all assume (by making $kT = hc/\lambda_0$) that the observed emission is tied uniquely to a single emitting annulus. In reality, each annulus emits as a blackbody, not at a single wavelength, so one observed wavelength corresponds to the combined emission from a suite of annuli. To get the effective flux-weighted mean emitting radius for any given wavelength, integrating over the surface brightness profile of the disk $B(T(R))$ at $R$ from some inner edge $R_0$ gives

$$\langle R_{\lambda_0} \rangle = \frac{\int_{R_0}^{R_{\lambda_0}} B(T(R))R^2dR}{\int_{R_0}^{R_{\lambda_0}} B(T(R))RdR}.$$
We account for this overlapping of fluxes by stating that the effective temperature at $\lambda_0$ is given by $kT = Xhc/\lambda_0$, where $X$ takes into account the range of different annuli sizes that contribute to the emission at wavelength $\lambda_0$. Propagating this change through the analysis above and allowing for $\kappa$ to be nonzero, we have

$$R_3 = \frac{1}{c} \left( \frac{Xhc}{kT} \right)^{4/3} \left[ \left( \frac{GM}{8\pi \sigma} \right) \left( \frac{L_{\text{Edd}}}{\eta c^2} \right) (3 + \kappa) \dot{m} \right]^{1/3}, \quad (6)$$

where now $R_3$ is this flux-weighted emitting radius. By performing the integral in Equation (5) and dividing this radius by the prediction from Equation (2), one finds

$$X = \frac{(R_{\lambda_0})}{R_{\lambda_0}}. \quad (7)$$

This corrective $X$ factor depends on both the wavelength of emission and the black hole mass. It is typically of order unity and was 2.49 for NGC 5548 for $\lambda_0 = 1367$ Å (Fausnaugh et al. 2016).

A number of quasar accretion disk sizes have been measured using gravitational microlensing. In quasar microlensing, the amplitude of the variability encodes the disk size (see, e.g., the review by Wambsganss 2001). At optical wavelengths, disk sizes appear to follow the $M_{\text{BH}}^{2/3}$ scaling expected for thin disks, but are larger in absolute size than predicted from Equation (2) by a factor of 2–3 in some cases (Morgan et al. 2010). There is also evidence from lensed quasars that the temperature profile $\beta$ may be smaller than the thin-disk prediction. Jiménez-Vicente et al. (2014) found that the best-fit profile was 0.8. While it will be feasible to expand these studies to hundreds of lenses in the era of the Large Synoptic Survey Telescope, lensed systems will always be a relatively rare subset of quasars.

An alternative technique for measuring accretion disk sizes is reverberation mapping (Blandford & McKee 1982; Peterson 1993; Wanders et al. 1997; Collier et al. 1998; Kriss et al. 2000; Sergeev et al. 2005). This was developed to measure the distance to the broad-line region by observing the time delay between variability in the continuum emission (as a proxy for the ionizing radiation from the innermost regions of the disk) and the response of the broad emission lines. This method can also be adapted to measure the relative time lag between the continuum emission at two wavelengths, e.g., two photometric bandpasses, which is then a proxy for the difference in the disk radii contributing to the emission (Equation (3)). This allows for estimating effective accretion disk sizes at those emitting wavelengths in unlensed quasars, and thus can be done on a much larger sample of objects. The primary challenge is that quasars show little variability on the short timescales corresponding to light travel times across the disk (e.g., MacLeod et al. 2010).

Early attempts at disk reverberation mapping include Wanders et al. (1997) and Collier et al. (1998) for NGC 7469 and Peterson et al. (1998) for NGC 4151. More recently, Sergeev et al. (2005) measured continuum lags at $2\sigma$ or upper limits for approximately a dozen objects. Interpreting the lags as light travel delays across the disk, the lags implied disk sizes growing as $L_{\text{obs}}^{0.4-0.5}$, close to their prediction of $L_{\text{obs}}^{0.5}$ from lags due to simple radiative propagation of variability (Sergeev et al. 2005). Shappee et al. (2014) and Fausnaugh et al. (2016) observed a wide range of wavelengths tracking the broadband variability of NGC 2617 and NGC 5548 (respectively) from the X-rays through the infrared. Both of these studies found the wavelength dependence of their accretion disk fits to be consistent with the thin-disk prediction of $\beta = 4/3$, with evidence that it may be closer to $\beta = 1$. Like some of the microlensing results, the accretion disk size estimates from these two studies were larger than predicted given the black hole mass estimates for these objects. In particular, the Space Telescope and Optical Reverberation Mapping (AGN STORM) campaign for NGC 5548 (e.g., De Rosa et al. 2015) is the highest-quality variability data set for a single object, and Edelson et al. (2015) and Fausnaugh et al. (2016) conclude that the accretion disk is roughly three times larger than expected from Equation (6), assuming an accretion at 10% of the Eddington rate. The Pan-STARRS collaboration performed a similar analysis for the griz bands on a sample of high-luminosity quasars. They restricted their work to two redshift bins that minimized broad emission line contamination to the optical filters and consistently find that the accretion disks are larger than expected from thin-disk theory (Jiang et al. 2017).

In this paper, we use data from the Dark Energy Survey (DES; Flaugher 2005; Dark Energy Survey Collaboration et al. 2016) to detect continuum time delays and study accretion disks in a sample of $z \geq 0.7$ quasars. In Section 2, we briefly describe the DES survey and data. In Section 3, we describe the analysis of our data and our methodologies. We conclude in Section 4.

## 2. Observations

DES is a five-year, five-band, optical, photometric survey covering 5000 square degrees of the southern sky, starting in 2013, using the Dark Energy Camera (Flaugher et al. 2015) on the Victor M. Blanco 4 m telescope near the Cerro Tololo Inter-American Observatory near La Serena, Chile. The primary goal of the survey is to investigate the expansion of the universe using weak lensing, baryon acoustic oscillations, galaxy clusters, and SNe Ia (Flaugher 2005; Flaugher et al. 2015). As part of the supernova search, 30 square degrees are be repeatedly observed on an approximately weekly cadence in the $g$, $r$, $i$, and $z$ filters for the duration of DES, amounting to 20–30 epochs per filter per year (Kessler et al. 2015). In these fields, we also have a set of spectroskopically verified quasars from the OzDES program (Australian DES/optical redshifts for DES; Yuan et al. 2015; Coldrass et al. 2017) as part of the DES and OzDES reverberation mapping project. This project photometrically and spectroskopically monitors 771 quasars in order to measure the masses of their SMBHs (King et al. 2015). These quasars are as faint as 23.6 in $g$ and were selected heterogeneously with a broad range of quasar detection techniques (e.g., Banerji et al. 2015; Tie et al. 2017). From the combination of these two surveys, we use the first three years of photometry and spectra for the 771 quasars that we continue to monitor (Diehl et al. 2016; Coldrass et al. 2017).

## 3. Analysis

We used the image subtraction pipeline developed for the analysis of supernova light curves (Goldstein et al. 2015; Kessler et al. 2015) to create our quasar light curves. We visually inspected the light curves for each of the approximately 800 reverberation mapping quasars in the DES SN fields that are part of the spectroscopic reverberation mapping...
all masses have an uncertainty of 0.4 dex, calculated using the McLure & Jarvis DES quasar sample analyzed in this work.

### Table 1
Sample Description

| Quasar Name        | R.A.          | Decl.       | z    | SN Field | BH Mass 10^6 M_s |
|--------------------|---------------|-------------|------|----------|-----------------|
| DES J025318.76+000014.20 | 43.32817      | 0.07061     | 1.56 | S1       | 0.49            |
| DES J024753.20-002137.69  | 41.97167      | -0.36047    | 1.44 | S1       | 1.17            |
| DES J021500.22-043007.49   | 33.75092      | -4.50208    | 1.01 | X1       | 0.38            |
| DES J022440.70-043567.60   | 36.16960      | -4.61600    | 0.91 | X3       | 0.20            |
| DES J022436.17-065912.30   | 36.15071      | -6.98675    | 1.36 | X2       | 0.52            |
| DES J022108.60-061753.20   | 35.28583      | -6.29811    | 1.22 | X2       | 0.77            |
| DES J022344.56-064039.00   | 35.93568      | -6.67750    | 0.98 | X2       | 0.06            |
| DES J033719.99-262418.83   | 54.33328      | -26.40523   | 1.17 | C1       | 1.01            |
| DES J024918.24-001730.98   | 42.32600      | -0.29194    | 1.24 | S1       | 0.49            |
| DES J024854.79+001054.12   | 42.22830      | 0.18170     | 1.15 | S1       | 0.90            |
| DES J024133.65-010724.20   | 40.39021      | -1.12339    | 1.87 | S2       | 0.79            |
| DES J024159.74-010512.41   | 40.49892      | -1.08678    | 0.90 | S2       | 0.61            |
| DES J021514.27-053321.31   | 33.80946      | -5.55592    | 0.70 | X1       | 0.04            |
| DES J024357.90-011330.40   | 40.99125      | -1.22511    | 0.90 | S2       | 0.14            |
| DES J021952.14-040919.91   | 34.96725      | -4.15553    | 0.69 | X1       | 0.66            |

**Note.** DES quasar sample analyzed in this work. “SN Field” denotes the supernova field in which the quasar resides (Flaugher 2005; Flaugher et al. 2015). Note that all masses have an uncertainty of 0.4 dex, calculated using the McLure & Jarvis (2002) relationship for Mg II.

We constructed our final list of 15 candidates as the subset of all quasars that had a substantial flux variation (≥5 times the photometric errors) on a timescale of weeks in both the g and z bands, excluding the first or last few data points of each observing season. This was to avoid variations that would occur in other bands that would require data before or after the DES observing season. These bands provide the longest wavelength baseline and represent the maximum (g) and minimum (z) levels of expected variability. Significant variability in both bands gives the best indication that we can recover a time delay.

Table 1 summarizes the general properties of the quasars in this final sample of 15 quasars that were classified as our best photometric lag candidates for having the highest photometric variability and multiband cadence around the feature(s). We derive lag results from the observations in the season in which the highest amplitude variability was observed. Five of the quasars exhibited strong variability in more than one season, and three showed it in all three seasons. For these sources, we analyze each season independently. The light curves, shown in Figures 1 and 2, and as Table 2, have on average 30 epochs per season and an average cadence of 6–8 nights between observations. All four bands are typically observed on the same night. We also note that one of our quasars, DES J024854.79+001054.12, is separated from a FIRST radio source by 0°9, and therefore some of its variability may arise from a jet rather than changes in the accretion disk. In some cases, we do not analyze multiple seasons because individual seasons show no evidence of variability.

#### 3.1. Lag Measurements

We use two separate analysis techniques to measure the time delays between the continuum bands. The first is the interpolated cross-correlation function (ICCF) method (Gaskell & Sparke 1986; Peterson et al. 2004), where two light curves are shifted along a grid of time lags and the cross-correlation coefficient r is calculated at each spacing (see Figure 1 of Gaskell & Sparke 1986). This method linearly interpolates between epochs to fill in missing data. A series of 1000 Monte Carlo runs re-sampling (with replacement) the light curves provide the uncertainty on the lag detection using the flux randomization/random subset replacement method, where the lag distribution is given by the mean of the distribution of cross-correlation centroids for which r > 0.8r_max.

For the second method, we used JAVELIN,69 which models quasar variability as a damped random walk (DRW; Zu et al. 2013). The DRW models quasar light curve behavior quite well on timescales of months to years (Gaskell & Peterson 1987; MacLeod et al. 2010; Zu et al. 2013), although there may be extra variability power on the much shorter timescales (tens of minutes compared to days) as seen in a group of quasars sampled by Kepler (Edelson et al. 2014; Kasliwal et al. 2015). JAVELIN has been used in previous emission line (e.g., Grier et al. 2012a, 2012b; Zu et al. 2013; Pei et al. 2017) and continuum (Shappee et al. 2014; Fausnaugh et al. 2016) reverberation mapping campaigns.

JAVELIN assumes that all light curves are shifted, scaled, and smoothed versions of the driving light curve. It uses the DRW model to carry out the interpolation between epochs. For this purpose, it is not essential that the DRW model exactly describes the true variability of the quasar—it needs only to be a reasonable approximation. The model has five parameters if fitting two light curves, a driver and shifted version: the DRW amplitude and timescale, the relative flux scale factor, the top-hat smoothing timescale, and the time lag. For relatively short, sparsely sampled light curves, it is not possible, either statistically or physically, to determine all of these parameters. Therefore, we restrict the damping timescale to 300 days, as has been found for a larger sample of quasars from the Sloan Digital Sky Survey (MacLeod et al. 2010).

JAVELIN also assumes that the measurement errors are well characterized and Gaussian, which can lead to underestimation of the uncertainties if either of these assumptions is incorrect. This has been noted in other studies (e.g., Fausnaugh et al. 2016), and we compare our lag distributions from JAVELIN to those obtained through the ICCF in Figure 3. The general trend is that the two methods are consistent with one another, with

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69 Available at https://bitbucket.org/rye17/javelin.
the centroids of the distributions for which \( r > 0.8r_{\text{max}} \) for the ICCF uncertainties that are generally larger. This has been noted in other works (e.g., Fausnaugh et al. 2016). Jiang et al. (2017) perform several tests on JAVELIN with one of their quasars by creating mock light curves with a known \( \delta \)-function shift from the original Pan-STARRS data and find that JAVELIN is able to recover the input delays below the cadence of the light curves, whereas the ICCF method does not. We report JAVELIN lags for the remainder of the paper.

We provide a summary of our lag posterior distributions in Table 3. Most of these lags are consistent with no time delay in the continuum emission at the 1\( \sigma \)–2\( \sigma \) level, but the wavelength-dependent offsets in many cases strongly suggest that an upper limit on the lag has been observed. We use these upper limits, based on the 2\( \sigma \) positive tail of the lag distributions, in all following analyses that use the individual JAVELIN lag data.

3.2. JAVELIN Thin-disk Model

We created an extension to JAVELIN, hereafter the JAVELIN thin-disk model, that directly fits the parameters of the thin-disk model, \( R_{\lambda} \) and \( \beta \), rather than getting these from an optimized fit to the individual time lags. This thin-disk model is now available for public use through the regular JAVELIN distribution. We note that this is the flux-weighted radius \( R_{\lambda} \) from Equation (6). To achieve this, we adapted JAVELIN to fit all of the continuum light curves simultaneously and find which \( R_{\lambda} \) and \( \beta \) values best reproduce the
lagged light curves from the driving light curve. The benefit of this approach is that it reduces the number of parameters and uses all of the photometric data to essentially produce a better sampled light curve. In the case where $\beta = 4/3$, the $R_{\lambda}$ parameter from Equation (3) or (6) sets the absolute size of the disk and depends on the quasar properties (mass, mass accretion rate, radiative efficiency, etc.), while $\beta$ corresponds to the temperature profile of the disk as a function of radius. If $\beta = 4/3$, this means that there is some heating term that does not scale as $1/R$. We tested these modifications to JAVELIN in two ways. First, the JAVELIN website provides a simulated 5-year quasar light curve, with an 8-day cadence and 180-day seasonal gaps to account for realistic seasonable inaccessibility, similar to what we expect at the end of DES. We used a grid of $R_{\lambda}$ and $\beta$ values to generate new light curves based on these simulated data with known lags between the bands. We then analyzed these simulated light curves to determine how well these values were recovered in several regimes. Most critically, we were interested in the performance when the light curve sampling rate was greater than, comparable to, and less than the shifts we applied using our known input thin-disk parameters for $R_{\lambda}$ and $\beta$. Recovery of these values works well in many cases, although it has some trouble recovering the model parameters in the instances with steep temperature profiles ($\beta > 3$) or disk light-crossing times $R_{\lambda}/c$ that are small compared to the sampling timescale ($<1/10$th of the cadence). Figure 4 shows the results of a test with $R_{\lambda} = 3.9$ lt-day and $\beta = 1.5$. In this test, the parameters are recovered for a temperature profile close to what is predicted by thin-disk theory and with a disk size of the driving light curve at slightly under half the sampling cadence of the data. We also reanalyzed the data from Fausnaugh et al. (2016) on NGC 5548. Fausnaugh et al. (2016) performed pairwise lag analyses on sets of Hubble Space Telescope (HST), Swift, and ground-based light curves to detect lags with respect to the HST 1367 Å light curve and then fit for $R_{1367}$ ($\alpha$ in that paper) and $\beta$. Those authors experimented with various subsets of the data, particularly subsets that excluded bands that may be contaminated by emission from other physical processes (e.g., broad emission lines or the Balmer continuum). We reanalyzed their data with our modified code and simultaneously fit a total of 17 light curves excluding the $U$ and $u$ bands due to Balmer continuum contamination and fixing the damping...
timescale at 164 days. The u- and U-band exclusions were adopted by Fausnaugh et al. (2016), and the damping timescale is based on previous, longer time baseline studies of NGC 5548 by Zu et al. (2011). Our result on the NGC 5548 data is consistent with the Fausnaugh et al. (2016) values with tighter constraints on \( R_{\text{H} \beta, \lambda} \) and \( \beta \) from fitting them directly, albeit now with a double solution, shown in Figures 5 and 6. The two solutions have a similar likelihood to one another and prefer smaller \( R_{\text{H} \beta, \lambda} \) and \( \beta \) values compared to those found in Fausnaugh et al. (2016). One of the two solutions is within the 1σ error contours from Fausnaugh et al. (2016). The double-peaked nature of our solution may be a product of the high dimensionality of parameter space in our model, and it is encouraging that we find a similar result as a different method.

### 3.2.1. DES Results

We then used this algorithm for the DES quasars that had yielded tentative \( r \), \( i \), and/or \( z \) lag measurements relative to the \( g \) band. We still restrict the DRW damping timescale to fall between 100 and 300 days for this analysis. We also fixed \( \beta = 4/3 \), as we found we were unable to provide good constraints on both \( R_{\text{H} \beta, \lambda} \) and \( \beta \) simultaneously for any object. This assumption is well motivated from theory, but we note that observations have shown evidence for a smaller \( \beta \) value closer to 0.8–1. If \( \beta \) is smaller than our assumption, this would inflate the final disk sizes somewhat. Figure 7 shows an example posterior distribution for \( R_{\text{H} \beta, \lambda} \) for DES J024918.24-001730.98 whose full posterior distributions for all model parameters is in Figure 8. Fits for the remainder of our objects can be found in the figure set.

As stated in Section 3, five objects in our current quasar sample have large amplitude variability in more than one DES observing season, and we compare their disk sizes with this method to check its performance. Two of these objects have disk sizes from three DES seasons, while the other three have only two analyzed seasons of variability. Figure 9 illustrates the \( R_{\text{H} \beta} \) values for each of these objects, and we see that they are all consistent at the 1σ–1.5σ level between the observing seasons. Different disk sizes between seasons could imply that the size uncertainties are underestimated, that the disk has undergone some structural change, or that the time delays are being influenced by emission that is not a simple reprocessing of emission from the inner regions of the disk.

One possible concern is contamination of the photometric bandpasses by emission line flux from larger scales. For the redshift range of our source DES (0.7 < \( z \) < 1.6), the Mg II emission line is present in the \( g \), \( r \), or \( i \) band, along with surrounding blends of Fe emission. The equivalent widths of the C IV line for luminous quasars like those in our sample are lower than for less-luminous Seyferts like NGC 5548 (the well-known Baldwin Effect; Baldwin 1977). We therefore expect emission line contamination to be less important for our quasars that have C IV emission within the DES bandpass (a small fraction of our sample) compared to AGN like NGC 5548. For the sample of Pan-STARRS quasars, with similarly high luminosity to those presented here, Jiang et al. (2017) find that the emission line contamination to continuum flux for their highest-confidence subsample is less than 6% and makes a negligible contribution to the lag signals. Using the OzDES coadded spectra, we find that the Mg II line contribution to the total flux in the DES bandpasses is roughly the same as was found in Jiang et al. (2017), about 1%–3% with a maximum of 7%. What matters for lag measurements for the accretion disk is that the strength of any line variability in the bandpass is much smaller than that of the continuum on short timescales. The line to continuum flux ratio is a reasonable proxy for this effect, although the relative line variability is often larger than the relative continuum variability.

### 3.3. Correlation with Black Hole Masses

To compare our disk sizes with previous studies, we require an estimate of the black hole mass. A reverberation mapping campaign is currently underway for these sources (see King et al. 2015 for a simulation of the DES reverberation mapping survey), which will provide the most accurate masses. For now, we use single-epoch mass estimates using the Mg II broad emission line from the OzDES coadded spectra and the relationship from McLure & Jarvis (2002). The OzDES spectra were calibrated using the DES photometry, and the emission line full-width half-maxima (FWHM) were measured using the IRAF split package. The resulting masses span more than an order of magnitude.

We compare our results to other studies in Figure 10. To meaningfully compare all objects at the same rest wavelength of 2500 Å, we assume that the effective accretion disk size scales as the predicted \( \beta = 4/3 \). Since the microlensing models output the radius where \( \lambda = \frac{h c}{\mu a T} \) and our photometric data are sensitive to the flux-weighted radius that we have parameterized as \( \lambda = \frac{X_{\text{FWHM}}}{\epsilon} \) in Equation (6), we inflate the microlensing results by \( X_{\text{FWHM}}^3 \), calculated from Equation (7) for each object individually, such that all of the quasar radii between the two methods are probing the same disk scale. Despite presenting our redshift-corrected individual lags results as upper limits derived from the 2σ positive tail of their lag distributions because the negative tails are consistent with no lag at the 1σ
level, they are fairly similar to measurements reported by other studies.

We then compared these $R_{500}$ constraints from our JAVELIN model to those derived from fitting the lags alone. Figure 11 shows these new size measurements alongside both literature values and those shown in Figure 10, and we provide a summary of these disk sizes in Table 3. Many of our quasar disk sizes are consistent with moderate ($\sim 0.3$) to super-Eddington accretion rates as well as the larger disk sizes of the previous literature given our uncertainties. While many of our measurements are on the lower end of previous disk sizes, the DES sample spans the same range of disk sizes as those found in the Pan-STARRS survey (Jiang et al. 2017). Both sets of disk sizes assume a temperature profile $\beta = 4/3$. The principle difference is that our method assumes a thin-disk structure from the outset and fits all light curves simultaneously. We sample the thin-disk parameters and use them to produce lagged light curves that are matched to the observed light curves and then evaluated on how well they reproduce the observations. This method does not fit for lags directly, instead they are produced from Equation (4) given our observed wavelengths and MCMC sampled model parameters. Previous works have instead fit for the lags first, pairwise with respect to the continuum, and then used the ensemble of lags with respect to the continuum to fit for a disk size. There is no immediately obvious reason why one method would produce systematically larger or smaller accretion disks than the other.

From Equation (2), we expect that the disk size should scale as $R_{500} \propto M^{2/3}$ in traditional thin-disk theory for a roughly fixed $L/L_{\text{Edd}}$, as has been found for luminous quasars (Kollmeier et al. 2006). We note, however, that X-ray studies (e.g., Aird et al. 2012), optical studies with well-characterized selection functions (e.g., Schulze & Wisotzki 2010), and phenomenological modeling (e.g., Weigel et al. 2017) argue that the Eddington ratio distribution of quasars is more power-law-like. There appears to be a weak trend with mass in Figure 11, albeit with a large scatter. It should be noted again that the uncertainties in the mass measurements for all of these quasars is roughly 0.4 dex. Prior accretion disk measurements, both through microlensing and photometric reverberation mapping, have found that many disks larger than expected from the thin-disk theory by a factor of a few (Morgan et al. 2010; Fausnaugh et al. 2016; Jiang et al. 2017). Given our large uncertainties, our objects are consistent with both these larger disk sizes as well as thin disks with moderate-to-high accretion rates. A small subset of our JAVELIN thin-disk models require Eddington ratios greater than unity, but our sample on the whole shows a large scatter around a thin disk with a moderate accretion rate.

One explanation for larger disk sizes is higher accretion rates for the black holes closer to the Eddington limit (Fausnaugh et al. 2016), but at these rates the disks would no longer remain thin. Another explanation provided by Hall et al. (2018) for large disks is that there could be a low-density atmosphere around the thin disk that modifies the optical and UV regions of the disk to
appear larger than they would as a blackbody spectrum. A third possibility is that quasars have high intrinsic reddening that has not been taken into account (Gaskell et al. 2004). This would make the quasars more luminous and naturally increase the expected disk sizes by a factor of a few. Depending on the exact magnitude of this correction, it could completely remove the discrepancy of the previously too large disk sizes (Gaskell 2017) and move the DES quasars to Eddington accretion rates of 0.1 or less. Gaskell et al. (2004) also find that the intrinsic reddening is greater for lower-luminosity objects, which would produce the largest discrepancy at the lowest luminosities. While Figure 11 plots the size versus black hole mass, the x-axis is a fair proxy for the luminosity. The objects on the left of the plot are those...
that would have the largest reddening correction and are currently the most discrepant from the prediction without it.

3.4. Stacking Analysis

After analyzing the individual lag distributions, we investigated whether a stronger signal could be found by combining the posterior distributions for quasars of similar properties. In the standard thin-disk model, the absolute size of the disk depends on the quasar properties. Thus, we expect that quasars with similar properties should have similar accretion disk sizes, and by combining their size distributions we may amplify the total signal. We divided our sample into two bins split at a mass of $6 \times 10^8 M_\odot$. This value gives approximately equal numbers

Figure 8. Corner plot for the full parameters for the quasar presented in Figure 3, DES J024918.24–001730.98 (Y1), in the JAVELIN thin-disk model analysis. As mentioned in the text, strong priors were placed on both the damping timescale $\tau$ and wavelength dependence $\beta$. The contours progress from $1\sigma$ to $3\sigma$ as they transition from black to lighter gray. The $R_{\text{in}}$ parameter is in units of light-days, whereas $\tau$ and all of the widths are in days. Note that all parameters are in the observed frame. Similar corner plots of the other quasars in the sample are available in the figure set. (The complete figure set (24 images) is available.)
of objects in each bin (7 and 8), albeit with different dynamic ranges of masses. The small mass bin covers an order of magnitude in mass, while the larger bin only a factor of two. Given the large systematic uncertainties in the single-epoch mass measurements, several of the objects could move between the bins with their mass errors, which could bias the stacked distributions. We rerun our JAVELIN thin-disk object again on each quasar individually without any priors on the parameters and then sum the accretion disk size likelihoods for all the quasars in the same bin after putting them in the rest frame and scaling them to the same reference wavelength (2500 Å) assuming $\beta = 4/3$. Figure 12 shows the final distributions for our mass bins, which are consistent with one another given the uncertainties. We expect a larger disk for higher-mass black holes, but the two distributions are roughly the same.

### Figure 9
Comparison of the JAVELIN disk model results for objects that have detections in multiple years. The three square blue points are the three quasars that have strong enough variability in two DES seasons to get two separate $R_{d0}$ measurements, whereas the black points are measurements for two quasars that have variability in all three seasons. Both of these quasars thus have two points on the plot, one comparing year 1 to year 2, and then another comparing year 1 to year 3. The diagonal dashed line is a 1:1 relation. The error bars represent the 1σ limits on the parameter distributions and show that the multiple years are roughly consistent with one another.

### Figure 10
Accretion disk size distribution at 2500 Å as a function of black hole mass. The two slanted lines correspond to the predictions from the thin-disk theory for an accretion disk inflated by a factor of $\lambda^{4/3}$ per the prescription in Fausnaugh et al. (2016) and found in Equation (6) at three different accretion rates relative to Eddington-0.1, 0.3, and 1. The DES sample is shown as upper limits based on the 95th percentile of the JAVELIN lag distributions as a conservative estimate given that several of our $g-r$ and $g-i$ lags were 2σ consistent with no lag. The black points are taken from gravitational lensing measurements of quasar accretion disk sizes (Morgan et al. 2010). As these were reported in units of the radius where $hc/kT = l$, they are similarly inflated to match the flux-weighted radius that is measured by the time-delay reverberation mapping data. The green points are the result of photometric reverberation mapping of NGC 5548 from the STORM campaign (Edelson et al. 2015; Fausnaugh et al. 2016) and NGC 2617 (Shappee et al. 2014), and the magenta for Pan-STARRS (Jiang et al. 2017). Note that we assumed that the disk’s size scaling as a function of wavelength, $\beta$, is 4/3 to put all the objects at the same rest wavelength.

### Figure 11
Disk size as a function of black hole mass, similar to Figure 10, but now with our disk sizes obtained from our new thin-disk JAVELIN extension as cyan squares. As before, all objects have been scaled to the flux-weighted radius in Equation (6) rather than the radius where $\lambda = \frac{hc}{kT}$.

### Figure 12
Stacked distribution of disk sizes at rest-frame 2500 Å assuming that $\beta = 4/3$. The two mass bins are divided at $6 \times 10^7 M_\odot$ to give roughly equal numbers in each bin, although the dynamic range of the higher-mass bin is smaller than the overall mass scaling uncertainties. We expect a larger disk for higher-mass black holes, but the two distributions are roughly the same.

### 4. Conclusion
We report quasar accretion disk size measurements using time delays between the DES photometric bandpasses as a
proxy for different radii in the disk. In addition to modeling the individual pairs of photometric bands, we present a new JAVELIN tool that fits a thin-disk model directly rather than to all of the available light curves simultaneously, which we test on both NGC 5548 and our DES quasars. Our results are as follows:

1. Even with the long cadence of the DES supernova pointings (≈1 week) compared to the few light-day expected size of the accretion disk, we are able to place meaningful upper limits on lags between continuum bands using JAVELIN for many of our objects. These limits are comparable to the sizes found for accretion disks through the gravitational lensing technique as well as other AGNs and quasars that have disk sizes derived in photometric reverberation mapping studies.

2. Our new extension of JAVELIN, a thin-disk model, is able to reproduce the AGN STORM result for NGC 5548 (Fausnaugh et al. 2016) by fitting for the thin-disk parameters directly rather than each lag individually. This new extension is publicly available as part of the JAVELIN package and should have many applications to future, multiwavelength time domain studies.

3. When we fix the β parameter at 4/3, we measure sizes for 15 DES quasars with this thin-disk model. The quasar sample spans almost two orders of magnitude in mass, and several of our measurements are of comparable precision to the disk lensing sizes. Given our large uncertainties for most of our sample, the disk size measurements are consistent with both the larger disks of previous results (Morgan et al. 2010; Shappee et al. 2014; Fausnaugh et al. 2016; Jiang et al. 2017) and with a thin disk accreting at a moderate rate compared to Edgington (≈0.3).

4. If quasars have a high intrinsic reddening, the larger disk sizes than those expected from thin-disk predictions can be accounted for as in Gaskell (2017).

5. We have five quasars with variability in multiple DES observing seasons and analyze each season of data independently with our thin-disk model extension to JAVELIN. In two of these quasars, we have variability in all three seasons. The accretion disk sizes are consistent with each other in all of these cases.

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