A POSSIBLE CARBON-RICH INTERIOR IN SUPER-EARTH 55 Cancri e

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ABSTRACT

Terrestrial planets in the solar system, such as the Earth, are oxygen-rich, with silicates and iron being the most common minerals in their interiors. However, the true chemical diversity of rocky planets orbiting other stars is yet unknown. Mass and radius measurements are used to constrain the interior compositions of super-Earths (exoplanets with masses of 1–10 $M_{\oplus}$), and are typically interpreted with planetary interior models that assume Earth-centric oxygen-rich compositions. Using such models, the super-Earth 55 Cancri e (mass 8 $M_{\oplus}$, radius 2 $R_{\oplus}$) has been suggested to bear an interior composition consisting of Fe, silicates, and an envelope ($\gtrsim$10% by mass) of supercritical water. We report that the mass and radius of 55 Cancri e can also be explained by a carbon-rich solid interior made of Fe, C, SiC, and/or silicates and without a volatile envelope. While the data allow Fe mass fractions of up to 40%, a wide range of C, SiC, and/or silicate mass fractions are possible. A carbon-rich 55 Cancri e is also plausible if its protoplanetary disk bore the same composition as its host star, which has been reported to be carbon-rich. However, more precise estimates of the stellar elemental abundances and observations of the planetary atmosphere are required to further constrain its interior composition. The possibility of a C-rich interior in 55 Cancri e opens a new regime of geochemistry and geophysics in extraterrestrial rocky planets, compared to terrestrial planets in the solar system.

Key words: planetary systems – planets and satellites: general – planets and satellites: individual (55 Cancri e)

1. INTRODUCTION

The recently discovered transiting super-Earth 55 Cancri e orbiting a nearby (naked eye) G8V star every 18 hours is one of the most favorable super-Earths for detailed characterization. The planet was originally discovered in a five-planet system by the radial velocity method which gave its minimum mass (McArthur et al. 2004; Fischer et al. 2008). However, the recent discovery of its transits across the host star (Winn et al. 2011; Demory et al. 2011) has made possible accurate measurements of its mass (8.37 $\pm$ 0.38 $M_{\oplus}$; Endl et al. 2012) and radius (2.04 $\pm$ 0.15 $R_{\oplus}$; Gillon et al. 2012), and hence constraints on its interior composition.

The interior of 55 Cancri e, inferred from its mass and radius, has been suggested to bear an interior composition made of iron, silicates, and an envelope ($\gtrsim$10% by mass) of supercritical water (Winn et al. 2011; Demory et al. 2011; Gillon et al. 2012). A water envelope is required to explain the mass and radius with an oxygen-rich interior composition. Given its mass, even a pure silicate interior with no iron content could only barely explain the observed radius. Consequently, a massive water envelope ($\gtrsim$10% by mass) over a rocky Earth-like interior has been required in the above studies to explain the radius of this highly irradiated super-Earth. Moreover, given the extreme stellar irradiation ($T \sim 2500$ K; Demory et al. 2012), the water has been suggested to be in a supercritical state in the planetary envelope.

The silicate-rich and water-rich interior of 55 Cancri e as suggested by previous studies is based on the assumption of an oxygen-rich interior, motivated by terrestrial planets in the solar system. However, several recent studies have suggested the possibility of carbon-rich extrasolar planets, both theoretically (Lodders 2004; Kuchner & Seager 2005; Bond et al. 2010; Madhusudhan et al. 2011b; Oberg et al. 2011; Mousis et al. 2012) and observationally (Madhusudhan et al. 2011a; Madhusudhan 2012). Motivated by these studies, in the present work we investigate if the observed mass and radius of 55 Cancri e may be explained by a carbon-rich interior.

The possibility of a carbon-rich interior in 55 Cancri e is also motivated by the composition of its host star. The host star 55 Cancri has been reported to be carbon-rich, with C/O = 1.12 $\pm$ 0.19 (Delgado Mena et al. 2010; E. Delgado Mena 2012, private communication) and metal-rich ([Fe/H] = 0.31 $\pm$ 0.04; Valenti & Fischer 2005; Mena et al. 2010), and has an age of 10.2 $\pm$ 2.5 Gyr (von Braun et al. 2011). However, the stellar C/O is less than 2$\sigma$ above the C/O of 0.8 required to form abundant carbon-rich condensates in protoplanetary environments. Furthermore, the C/O ratio could be overestimated due to systematic errors in estimating the C and O abundances (Fortney 2012). However, if the central value of C/O = 1.12 is taken at face value (see, e.g., Carter-Bond et al. 2012) and the protoplanetary disk is assumed to mimic the stellar abundances, then the super-Earth 55 Cancri e would indeed be expected to have accreted substantial amounts of carbon-rich material, such as SiC and C, and be depleted in H$_2$O ice (e.g., Larimer 1975; Bond et al. 2010; Johnson et al. 2012).

In what follows, we first present, in Section 2, internal structure models of 55 Cancri e and constraints on its interior composition based on its observed mass and radius. In Section 3, we present thermochemical calculations exploring the possible compositions of planetesimals that may have formed 55 Cancri e. We discuss the implications of our results and future work in Section 4.

2. INTERIOR COMPOSITION

2.1. Internal Structure Model

We model the internal structure of the super-Earth 55 Cancri e, and use its observed mass and radius to constrain the chemical
composition of its interior. Our model solves the three canonical equations of internal structure for solid planets, namely, (1) mass conservation, (2) hydrostatic equilibrium, and (3) the equation of state (EOS; e.g., Fortney et al. 2007; Seager et al. 2007; Sotin et al. 2007; Valencia et al. 2007; Rogers & Seager 2010). In each spherical shell of the planet, the equations for mass and pressure balance form a system of two coupled differential equations, given by

\[ \frac{dr}{dM_r} = \frac{1}{4\pi r^2 \rho} \quad \text{and} \quad (1) \]

\[ \frac{dP}{dM_r} = -\frac{GM_r}{4\pi r^4}. \quad (2) \]

Here, we have adopted the mass interior to each spherical shell \( M_r \) as the independent variable, and we numerically solve for the radius \( r \) and pressure \( P \). The density \( \rho \) is related to the pressure \( P \) and temperature \( T \) via the EOS of the material, \( P = P(\rho, T) \). We adopt room-temperature EOSs for the species considered in this work, since mass–radius relations of solid exoplanets are known to be insensitive to temperature dependence in the EOS (see, e.g., Seager et al. 2007). For H\(_2\)O, MgSiO\(_3\) (perovskite), Fe, and SiC, we use the Birch–Murnaghan (Birch 1952) EOSs compiled in Seager et al. (2007). Our Birch–Murnaghan EOS for carbon comprises the graphite EOS (Wang et al. 2012) at low pressures, incorporates the phase transition (Bundy et al. 1996) from graphite to diamond at 10 GPa, and asymptotes to the Thomas–Fermi–Dirac EOS (Salpeter & Zapolsky 1967) for \( P \) > 1000 GPa. For diamond, we adopt the EOS from Dewaele et al. (2008). We assume that the planet is spherically symmetric, but is vertically differentiated into up to three chemically distinct regions, depending on the species under consideration. The mass fractions of the three regions are given as \( x_i = M_i/M_p \), \( i = [1–3] \), such that \( x_1 + x_2 + x_3 = 1 \). \( M_p \) is the total mass of the planet and \( M_i \) is the mass of each of the three layers.

We solve the system of equations simultaneously using a fourth-order Runge–Kutta scheme. The inputs to the model are the total mass of the planet \( (M_p) \) and the mass fractions of two of the three different regions, i.e., \( x_1 \) and \( x_2, x_3 \) is obtained from mass conservation, \( x_3 = 1 - x_1 - x_2 \). We start with the upper boundary \( (M_r = M_p) \) and integrate downward in mass until \( M_r = 0 \). The upper boundary conditions, which serve as initial conditions, are

\[ r \rightarrow R_p \text{ for } M_r \rightarrow M_p, \quad (3) \]

\[ P \rightarrow 0 \text{ for } M_r \rightarrow M_p, \quad (4) \]

and the lower boundary condition is

\[ r \rightarrow 0 \text{ for } M_r \rightarrow 0. \quad (5) \]

We use our model in two ways. First, we study mass–radius relations for planets with homogeneous compositions. In such cases, \( x_1 = 1 \) and \( x_2 = x_3 = 0 \). We choose a grid in \( M_p \), and for each \( M_p \) we compute the corresponding \( R_p \) for the given composition. Since \( R_p \) is required for the initial conditions but is not known a priori, we use a bisection root finder to solve for \( R_p \) iteratively, such that the lower boundary condition is satisfied. Second, we also use our model to determine constraints on the heterogeneous interior composition of 55 Cancri e given its observed \( M_p \) and \( R_p \). Here, we explore a fine grid in \( x_1 \)–\( x_2 \) space to constrain the regions that match \( M_p \) and \( R_p \) within their observational uncertainties.

### 2.2. Mass–Radius Relations

Figure 1 shows mass–radius relations for homogeneous planets of different compositions (i.e., \( x_1 = 1, x_2 = x_3 = 0 \)) along with data for several super-Earths. Super-Earths with radii above the H\(_2\)O curve likely host gaseous envelopes, since even purely ice compositions will not be able to explain their
radii. However, those below the $\text{H}_2\text{O}$ curve can be explained by various combinations of minerals, depending on whether an O-rich or C-rich composition is assumed. An important exception is noticed for planets such as 55 Cancri e, with radii between the silicate and carbon curves. In such cases, assuming O-rich compositions would mean that the planet possesses a volatile (e.g., $\text{H}_2\text{O}$) layer, since even a purely silicate composition would not explain the radius, as suggested in previous studies (e.g., Gillon et al. 2012). Whereas, if one allows for C-rich compositions, the same mass and radius could also be explained by purely solid planets with SiC and C based interiors without a volatile layer, as can be seen in Figure 1.

2.3. Constraints on Interior Composition

In what follows, we determine the constraints placed by the mass and radius of 55 Cancri e on the composition space of carbon-rich models of its interior. Interiors of carbon-rich planets are expected to be composed of iron (Fe), carbon (C), SiC, and/or silicates, depending on the thermal conditions where the planetesimals originated (Kuchner & Seager 2005; Bond et al. 2010; Carter-Bond et al. 2012; also see Section 3). Consequently, we consider two model families with distinct compositions: Fe–SiC–C and Fe–MgSiO$_3$–C. Our planetary interior model in each case is comprised of three regions ordered by bulk density, an Fe core, overlaid by a layer of SiC or MgSiO$_3$ (perovskite), and an uppermost layer of carbon. In each case, Fe–SiC–C or Fe–MgSiO$_3$–C, we constrain the mass fractions of the three regions that explain the observed mass and radius of 55 Cancri e.

Figure 2 shows a ternary diagram of the possible compositions of 55 Cancri e which explain its observed mass and radius within their observational uncertainties. We adopt the latest estimate of its mass, $M = 8.37 \pm 0.38 \, M_{\odot}$ (Endl et al. 2012), and two values for its radius, $R_p = 2.04 \pm 0.15 \, R_{\oplus}$ in the visible (Winn et al. 2011; Gillon et al. 2012), and $R_p = 2.20 \pm 0.12 \, R_{\oplus}$ for a gray radius obtained by combining the visible and infrared (4.5 $\mu$m) radii (Demory et al. 2011; Gillon et al. 2012). The red region (which includes the blue region) in Figure 2 shows constraints from the visible radius, and the blue region which is a subset of the red region shows the constraints from the gray radius.

Figure 3(a) shows the constraints on the mass fractions for the Fe–SiC–C class of solutions. A wide range of carbon-rich interior compositions can explain the observed mass and radius of 55 Cancri e. The visible radius places an upper limit of 41% on the Fe mass fraction, but allows a wide range of (SiC, C) combinations. If an Earth-like Fe core mass (33%) or less is assumed, then the visible radius allows a differentiated mantle comprising of all possible proportions of SiC and C, constrained only by mass conservation ($x_1 + x_2 + x_3 = 1$, see Section 2.1). For example, extreme combinations of (Fe, SiC, C) = (33%, 67%, 0%) and (33%, 0%, 67%) are both possible. However, intermediate compositions such as (33%, 33%, 34%) may be more representative of the true composition, since over the long planet formation timescales (Gyr) all the three species are likely to be abundant enough to contribute to planetesimal compositions in the inner nebular ($a \lesssim 1.2$ AU) where the Fe–SiC–C type of planets are more likely to be formed (see, e.g., Section 3 and Bond et al. 2010).

On the other hand, considering the gray radius narrows down the solution space, requiring a maximum of 18% Fe by mass, the SiC and C fractions allowed depend on the Fe mass fraction. Considering Fe = 10%, for example, a minimum of 70% C is required, with SiC < 20%. For Fe < 5%, however, all possible combinations of SiC and C are allowed, such that SiC + C < 95%. We note, however, that the Fe content derived from the gray radius may only be a lower limit. The infrared radius may contain atmospheric molecular absorption, making it slightly larger than the visible radius. Such absorption may be caused by an atmosphere ($\sim$1000 km) of varied compositions, between just 2 scale heights ($R_{\text{H}}$) of a metal-rich H$_2$-dominated atmosphere and 30 $R_{\text{H}}$ of a CO-dominated atmosphere (see, e.g., Figure 7 of Gillon et al. 2012). New spectral data would be required to precisely constrain this possibility.
Figure 3(b) shows the constraints on the mass fractions for the Fe–MgSiO$_3$–C class of solutions. Considering an Earth-like Fe content of 33%, the visible radius allows for a maximum of 20% MgSiO$_3$, requiring over 47% C, which is expected given the Fe content of 33%, and are likely extreme, if not unphysical, (also see Gillon et al. 2012), particularly considering that the host star has a supersolar metallicity ([Fe/H] = 0.31 ± 0.04; Valenti & Fischer 2005). However, even a C mass fraction of 10% is two orders of magnitude higher than that in the Earth, which has less than 0.1% C by mass (McDonough & Sun 1995).

3. FORMATION CONDITIONS AND PLANETESIMAL COMPOSITIONS

A carbon-rich 55 Cancri e may also be tentatively consistent with the composition of the host star. We investigate the possible formation conditions of 55 Cancri e assuming that the reported stellar abundances represent those of its primordial disk (see Sections 1 and 4 for challenges in this assumption). We adopt the abundances of the host star reported by Delgado Mena et al. (2010), following Carter-Bond et al. (2012). Given the thermodynamic conditions in the disk mid-plane, we compute the condensate chemistry in multi-phase chemical equilibrium using the commercial software HSC Chemistry.

We model the protoplanetary disk using a thin disk model based on the prescription of Shakura & Sunyaev (1973), with a turbulent viscosity given by $\nu_t = \alpha C_S^2/\Omega$, where $C_S$ is the local sound velocity, $\Omega$ is the Keplerian rotation frequency, and $\alpha$ is the dimensionless viscosity parameter. Our model incorporates the opacity law developed by Ruden & Pollack (1991) (see, e.g., Drouart et al. 1999 for details). The temporal evolution of the disk temperature, pressure, and surface density profiles depends upon the evolution of the accretion rate, $\dot{M}$, which we define (following Makalkin & Dorofeeva 1991) to be $\dot{M} = M_0(1 + t/t_0)^{-3}$, where $M_0$ is the initial accretion rate, and $t_0$ is the accretion timescale. We adopt $\alpha = 1.5$, a value that is consistent with the evolution of accretion rates in circumstellar disks (Hartmann et al. 1998). The accretion timescale $t_0$ is calculated based on Makalkin & Dorofeeva (1991) as $t_0 = R_D^2/3 \nu_D$, where $\nu_D$ is the turbulent viscosity at the initial radius of the sub-disk, $R_D$. Three parameters constrain $M_0$ and $t_0$: the initial mass of the disk $M_{D0}$, the coefficient of turbulent viscosity $\alpha$, and the radius of the sub-nubela $R_D$. In the present case, we have adopted the parameters used by Kavelaars et al. (2011) for their nominal solar nebula model, i.e., $\alpha = 0.003$, $R_{D0} = 15$ AU, and $M_{D0} = 0.06 M_\odot$.

The refractory condensate composition as a function of the temperature ($T$) is shown in Figure 3. At high temperatures ($T > 1100$ K), SiC and Fe are the most dominant condensates. As the temperatures cool to between 700 and 1100 K, pure carbon (as graphite) becomes the most dominant condensate, followed by Fe and silicates, e.g., Mg$_2$SiO$_4$. However, at low temperatures, $T$ below 700 K, Mg$_2$SiO$_4$ dominates the condensate composition, despite the high C/O ratio (also see Bond et al. 2010; Carter-Bond et al. 2012). Figure 1 also shows representative orbital separations ($a$) in the protoplanetary disk and their corresponding temperatures at different epochs in the disks evolution. For $a \lesssim 1.2$ AU in the disk, SiC, Fe, and C condense early in the disks lifetime, and hence dominate the planetesimal composition. For $a \sim 1.2$–1.6 AU, graphite far
dominates the planetesimal composition, followed by Fe and Mg$_2$SiO$_4$. At lower temperatures, however, for $a \gtrsim 1.6$ AU, Mg$_2$SiO$_4$ dominates the planetesimal composition.

Depending on whether the planetesimals that formed 55 Cancri e originated primarily within or beyond $\sim 1.2$ AU, its interior can bear end-member compositions of Fe–SiC–C or Fe–silicates–C, respectively, or an intermediate composition. Since the protoplanet likely formed farther than the planet’s current orbital separation ($0.015$ AU) and migrated in, it likely accreted substantial amounts of Fe-rich and C-rich condensates irrespective of its original location. On the other hand, it is unlikely that the planet formed in situ because the disk temperatures at this location prevent the condensation of dominant refractory condensates.

4. DISCUSSION

We show that the sum total of available data, including the planetary mass and radius, and the stellar abundances, supports the possibility of a carbon-rich interior in 55 Cancri e. Numerous studies have suggested the possibility of carbon-rich exoplanets, both theoretically (e.g., Kuchner & Seager 2005; Bond et al. 2010; Madhusudhan et al. 2011b) and observationally (Madhusudhan et al. 2011a; Madhusudhan 2012). However, the prevalent practice is to assume Earth-centric compositions, comprising Fe, silicates, and H$_2$O, in explaining super-Earth observations. A carbon-rich 55 Cancri e would represent a departure from Earth-centric mineralogies in rocky exoplanets. Nevertheless, follow-up efforts are required to confirm a carbon-rich 55 Cancri e.

High confidence elemental abundances of the host star can help refine the constraints on the formation conditions of 55 Cancri e. Given currently reported abundances, a C/O $\geq 0.8$, required to form C-rich refractories (Larimer 1975), holds only at $\sim 2\sigma$ and the C/O ratio may also have been overestimated (Fortney 2012). Furthermore, we assume that the protoplanetary disk bears the same composition as the host star. While this may be a reasonable assumption for deriving refractory compositions of planetesimals forming rocky planets (see, e.g., Bond et al. 2010; Carter-Bond et al. 2012; Johnson et al. 2012), the possibility of local perturbations in the C/O ratio of the disk may not be entirely ruled out; i.e., the possibility that carbon-rich planets may form around oxygen-rich stars and vice versa (Kuchner & Seager 2005; Madhusudhan et al. 2011b; Oberg et al. 2011). In particular, carbon-rich gas giant planets may form by predominantly accreting effectively carbon-rich gas in regions beyond the water-ice condensation line in an oxygen-rich disk (Oberg et al. 2011).

High-precision spectroscopy in the future may also be able to constrain the presence of an atmosphere in 55 Cancri e and its composition. Currently, both reported radii, visible and infrared, are consistent at the $1\sigma$ uncertainties, though the latter is slightly larger (Gillon et al. 2012). Excess infrared absorption may be caused by molecular species and/or collision-induced absorption (Miller-Ricci et al. 2009), which could be constrained by future observations.

A carbon-rich interior in 55 Cancri e has far-reaching implications for geophysical processes in its interior. Earth’s interior is oxygen-rich, with carbon less than 0.1% by mass (McDonough & Sun 1995), in contrast to a carbon-rich interior of 55 Cancri e. Both carbon and SiC have over two orders of magnitude higher thermal conductivities than the silicates and oxides that dominate Earth’s mantle (Goldberg et al. 2001), implying that the thermal evolution of 55 Cancri e may be different from that of oxygen-rich planets. The high thermal conductivities, compounded with the paucity of water, may influence the likelihood of plate tectonics in carbon-rich super-Earths (Valencia et al. 2007; Korenaga 2010), though new measurements of viscosity of carbon-rich materials at high pressures and high temperatures are required to constrain this possibility. A carbon-rich 55 Cancri e bolsters the idea that rocky exoplanets may be diverse in their chemical compositions and, hence, in their geophysical conditions.

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