Measurement of CP-Violation Parameter sin 2φ₁
with 152 Million BBAR Pairs

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(The Belle Collaboration)
Abstract

We present a precise measurement of the standard model CP-violation parameter $\sin 2\phi_1$ based on a sample of $152 \times 10^6$ $B\bar{B}$ pairs collected at the $\Upsilon(4S)$ resonance with the Belle detector at the KEKB asymmetric-energy $e^+e^-$ collider. One neutral $B$ meson is reconstructed in a $J/\psi K^0_S$, $\psi(2S) K^0_S$, $\chi_c K^0_S$, $\eta_c K^0_S$, $J/\psi K^*0$, or $J/\psi K^0_L$ CP-eigenstate decay channel and the flavor of the accompanying $B$ meson is identified from its decay products. From the asymmetry in the distribution of the time interval between the two $B$ meson decay points, we obtain $\sin 2\phi_1 = 0.733 \pm 0.057{\text{(stat)}} \pm 0.028{\text{(syst)}}$.

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In the standard model (SM), \(CP\) violation arises from an irreducible phase in the weak interaction quark-mixing matrix [Cabibbo-Kobayashi-Maskawa (CKM) matrix] \(^1\). In particular, the SM predicts a \(CP\)-violating asymmetry in the time-dependent rates for \(B^0\) and \(\bar{B}^0\) decays to a common \(CP\) eigenstate \(f_{CP}\), where the transition is dominated by the \(b \to c\bar{c}s\) process, with negligible corrections from strong interactions \(^3\):

\[
A(t) \equiv \frac{\Gamma(\bar{B}^0 \to f_{CP}) - \Gamma(B^0 \to f_{CP})}{\Gamma(\bar{B}^0 \to f_{CP}) + \Gamma(B^0 \to f_{CP})} = -\xi_f \sin 2\phi_1 \sin(\Delta m_d t),
\]

where \(\Gamma(B^0, \bar{B}^0 \to f_{CP})\) is the rate for \(B^0\) or \(\bar{B}^0\) to \(f_{CP}\) at a proper time \(t\) after production, \(\xi_f\) is the \(CP\) eigenvalue of \(f_{CP}\), \(\Delta m_d\) is the mass difference between the two \(B^0\) mass eigenstates, and \(\phi_1\) is one of the three interior angles of the CKM unitarity triangle, defined as \(\phi_1 \equiv \pi - \arg(V^*_{tb}V_{td}/V^*_{cb}V_{cd})\). Non-zero values for \(\sin 2\phi_1\) have been reported by the Belle and BaBar collaborations \(^3\), \(^4\), \(^5\), \(^6\).

Belle’s latest published measurement of \(\sin 2\phi_1\) is based on a 78 fb\(^{-1}\) data sample (data set I) containing \(85 \times 10^6\) \(B\bar{B}\) pairs produced at the \(\Upsilon(4S)\) resonance. In this paper, we report an improved measurement incorporating an additional 62 fb\(^{-1}\) (data set II) for a total of 140 fb\(^{-1}\) (\(152 \times 10^6\) \(B\bar{B}\) pairs). Changes exist in the analysis with respect to our earlier result \(^4\). We apply a new proper-time interval resolution function that reduces systematic uncertainties in \(\sin 2\phi_1\) and also in \(\Delta m_d\) and lifetime \((\tau_{B^0}, \tau_{B^{+}})\) measurements. We introduce \(b\)-flavor-dependent wrong-tag fractions to accommodate possible differences between \(B^0\) and \(\bar{B}^0\) decays. We also adopt a multi-parameter fit to the flavor-specific control samples to obtain the resolution parameters and wrong-tag fractions simultaneously. There are other improvements in the estimation of background components, which become possible with increased statistics.

The data were collected with the Belle detector \(^6\) at the KEKB asymmetric collider \(^7\), which collides 8.0 GeV \(e^-\) on 3.5 GeV \(e^+\) at a small (\(\pm 11\) mrad) crossing angle. We use events where one of the \(B\) mesons decays to \(f_{CP}\) at time \(t_{CP}\), and the other decays to a self-tagging state \(f_{tag}\), which distinguishes \(B^0\) from \(\bar{B}^0\), at time \(t_{tag}\). The \(CP\) violation manifests itself as an asymmetry \(A(\Delta t)\), where \(\Delta t\) is the proper time interval between the two decays: \(\Delta t \equiv t_{CP} - t_{tag}\). At KEKB, the \(\Upsilon(4S)\) resonance is produced with a boost of \(\beta\gamma = 0.425\) nearly along the \(z\) axis defined as anti-parallel to the positron beam direction, and \(\Delta t\) can be determined as \(\Delta t \approx \Delta z/(\beta\gamma)c\), where \(\Delta z\) is the \(z\) distance between the \(f_{CP}\) and \(f_{tag}\) decay vertices, \(\Delta z \equiv z_{CP} - z_{tag}\). The average value of \(\Delta z\) is approximately 200 \(\mu m\).

The Belle detector \(^6\) is a large-solid-angle spectrometer that includes a silicon vertex detector (SVD), a central drift chamber (CDC), an array of aerogel threshold Čerenkov counters (ACC), time-of-flight (TOF) scintillation counters, and an electromagnetic calorimeter comprised of CsI(Tl) crystals (ECL) located inside a superconducting solenoid coil that provides a 1.5 T magnetic field. An iron flux-return located outside of the coil is instrumented to detect \(K_L^0\) mesons and to identify muons (KLM).

We reconstruct \(B^0\) decays to the following \(CP\) eigenstates \(^8\): \(J/\psi K_S^0\), \(\psi(2S)K_S^0\), \(\chi_c K_S^0\), \(\eta_c K_S^0\) for \(\xi_f = -1\) and \(J/\psi K_L^0\) for \(\xi_f = +1\). We also use \(B^0 \to J/\psi K^{*0}\) decays where \(K^{*0} \to K_S^0\pi^0\). Here the final state is a mixture of even and odd \(CP\), depending on the relative orbital angular momentum of the \(J/\psi\) and \(K^{*0}\). We find that the final state is primarily \(\xi_f = +1\); the \(\xi_f = -1\) fraction is \(0.19 \pm 0.02\text{(stat)} \pm 0.03\text{(syst)}\) \(^8\).

The reconstruction and selection criteria for all \(f_{CP}\) channels used in the measurement are described in detail elsewhere \(^3\). \(J/\psi\) and \(\psi(2S)\) mesons are reconstructed via their
decays to $\ell^+\ell^-$ ($\ell = \mu, e$). The $\psi(2S)$ is also reconstructed via $J/\psi\pi^+\pi^-$, and the $\chi_{c1}$ via $J/\psi\gamma$. The $\eta_c$ is detected in the $K^0_S K^-\pi^+$, $K^+K^-\pi^0$, and $p\bar{p}$ modes. For the $J/\psi K^0_S$ mode, we use $K^0_S \rightarrow \pi^+\pi^-$ and $\pi^0\pi^0$ decays; for other modes we only use $K^0_S \rightarrow \pi^+\pi^-$. For reconstructed $B \rightarrow f_{CP}$ candidates other than $J/\psi K^0_L$, we identify $B$ decays using the energy difference $\Delta E \equiv E_{B}^{\text{cms}} - E_{\text{beam}}^{\text{cms}}$ and the energy-constrained mass $M_{\text{BC}} \equiv \sqrt{(E_{\text{beam}}^{\text{cms}})^2 - (p_{B}^{\text{cms}})^2}$, where $E_{\text{beam}}^{\text{cms}}$ is the beam energy in the center-of-mass system (cms) of the $\Upsilon(4S)$ resonance, and $E_{B}^{\text{cms}}$ and $p_{B}^{\text{cms}}$ are the cms energy and momentum of the reconstructed $B$ candidate, respectively.

Candidate $B^0 \rightarrow J/\psi K^0_L$ decays are selected by requiring ECL and/or KLM hit patterns that are consistent with the presence of a shower induced by a $K^0_L$ meson. The centroid of the shower is required to be within a 45$^\circ$ cone centered on the $K^0_L$ direction inferred from two-body decay kinematics and the measured four-momentum of the $J/\psi$.

We perform a multi-parameter fit to flavor-specific control samples to obtain wrong-tag fractions and parameters for the resolution function simultaneously. We select $B^0 \rightarrow D^*\ell^+\bar{\nu}_\ell$, $J/\psi K^0_S(K^+\pi^-)$, $D^{*-}\pi^+$, $D^{*-}\pi^-$, $D^{*-}\rho^+$, and $J/\psi K^0_S(\ell^+\ell^-)$ (for resolution parameters only) for $B^0$ decays, and $B^+ \rightarrow \Upsilon(2S)\pi^+$ and $J/\psi K^0_L$ for $B^+$ decays. The total numbers of candidates ($N_{\text{ev}}$) and purities ($p$) are $N_{\text{ev}} = 124118$ and $p = 0.82$ for $B^0$ decays, and $N_{\text{ev}} = 57305$ and $p = 0.81$ for $B^+$ decays. The fit uses free parameters for wrong-tag fractions (12), for the resolution function (14), for the $B^+$ background in $B^0$ decays (3), $\Delta m_d$, $\tau_{B^0}$ and $\tau_{B^+}$. The total number of parameters in the fit is 32. We add two parameters to the resolution function described in [10] to obtain an improved description of the effect of charmed particle decays in the $f_{\text{tag}}$ vertex. We test the new fit method and parameterization with a large number of Monte Carlo (MC) events. A fit to the MC control sample yields $\Delta m_d = (0.488 \pm 0.002)$ ps$^{-1}$, $\tau_{B^0} = (1.539 \pm 0.003)$ ps and $\tau_{B^+} = (1.679 \pm 0.004)$ ps for the input values of $\Delta m_d = 0.489$ ps$^{-1}$, $\tau_{B^0} = 1.541$ ps and $\tau_{B^+} = 1.674$ ps, respectively. The obtained wrong-tag fractions are also found to be correct. The unbinned maximum-likelihood fit to data yields $\Delta m_d = [0.511 \pm 0.005(\text{stat})]$ ps$^{-1}$, $\tau_{B^0} = [1.533 \pm 0.008(\text{stat})]$ ps and $\tau_{B^+} = [1.634 \pm 0.011(\text{stat})]$ ps, where the errors are statistical only. The results are consistent with the present world average values [11].

Charged leptons, pions, kaons, and $\Lambda$ baryons that are not associated with a reconstructed CP eigenstate decay are used to identify the $b$-flavor of the accompanying $B$ meson. The tagging algorithm is identical to the one used in reference [4]. We use two parameters, $q$ and $r$, to represent the tagging information. The first, $q$, has the discrete value +1 (-1) when the tag-side $B$ meson is likely to be a $B^0$ ($\bar{B}^0$), and the parameter $r$ is an event-by-event Monte Carlo-determined flavor-tagging dilution parameter that ranges from $r = 0$ for no flavor discrimination to $r = 1$ for an unambiguous flavor assignment. It is used only to sort data into six intervals of $r$, according to estimated flavor purity. We determine directly from data the average wrong-tag probabilities, $w_l \equiv (w^+_l + w^-_l)/2$ ($l = 1, 6$), and differences between $B^0$ and $\bar{B}^0$ decays, $\Delta w_l \equiv w^+_l - w^-_l$, where $w_l^{\pm(-)}$ is the wrong-tag probability for the $B^0(\bar{B}^0)$ decay in each $r$ interval. The event fractions and wrong-tag fractions are summarized in Table I. The total effective tagging efficiency is determined to be $\epsilon_{\text{eff}} \equiv \sum_{i=1}^{6} \epsilon_i (1 - 2w_i)^2 = 0.287 \pm 0.005$, where $\epsilon_i$ is the event fraction for each $r$ interval. The error includes both statistical and systematic uncertainties.

The vertex position for the $f_{CP}$ decay is reconstructed using leptons from $J/\psi$ decays or charged hadrons from $\eta_c$ decays, and that for $f_{\text{tag}}$ is obtained with well reconstructed tracks that are not assigned to $f_{CP}$. Tracks that are consistent with coming from a $K^0_S \rightarrow \pi^+\pi^-$...
TABLE I: The event fractions $\epsilon_l$, wrong-tag fractions $w_l$, wrong-tag fraction differences $\Delta w_l$, and average effective tagging efficiencies $\epsilon_{\text{eff}}^l = \epsilon_l(1 - 2w_l)^2$ for each $r$ interval. The errors include both statistical and systematic uncertainties. The event fractions are obtained from the $J/\psi K^0_S$ simulation.

| $l$ | $r$ interval | $\epsilon_l$ | $w_l$ | $\Delta w_l$ | $\epsilon_{\text{eff}}^l$ |
|-----|-------------|-------------|------|-------------|----------------|
| 1   | 0.000 – 0.250 | 0.398       | 0.464 ± 0.006 | -0.011 ± 0.006 | 0.002 ± 0.001 |
| 2   | 0.250 – 0.500 | 0.146       | 0.331 ± 0.008 | +0.004 ± 0.010 | 0.017 ± 0.002 |
| 3   | 0.500 – 0.625 | 0.104       | 0.231 ± 0.009 | -0.011 ± 0.010 | 0.030 ± 0.002 |
| 4   | 0.625 – 0.750 | 0.122       | 0.163 ± 0.008 | -0.007 ± 0.009 | 0.055 ± 0.003 |
| 5   | 0.750 – 0.875 | 0.094       | 0.109 ± 0.007 | +0.016 ± 0.009 | 0.057 ± 0.002 |
| 6   | 0.875 – 1.000 | 0.136       | 0.020 ± 0.005 | +0.003 ± 0.006 | 0.126 ± 0.003 |

decay are not used. Each vertex position is required to be consistent with the interaction region profile, determined run-by-run, smeared in the $r$-$\phi$ plane to account for the $B$ meson decay length. With these requirements, we are able to determine a vertex even with a single track; the fraction of single-track vertices is about 10% for $z_{CP}$ and 22% for $z_{\text{tag}}$. The proper-time interval resolution function $R_{\text{sig}}(\Delta t)$ is formed by convolving four components: the detector resolutions for $z_{CP}$ and $z_{\text{tag}}$, the shift in the $z_{\text{tag}}$ vertex position due to secondary tracks originating from charmed particle decays, and the kinematic approximation that the $B$ mesons are at rest in the cms. A small component of broad outliers in the $\Delta z$ distribution, caused by mis-reconstruction, is represented by a Gaussian function. We determine fourteen resolution parameters from the aforementioned fit to the control samples. We find that the average $\Delta t$ resolution is $\sim 1.43$ ps (rms). The width of the outlier component is determined to be $(39 \pm 2)$ ps; the fractions of the outlier components are $(2.1 \pm 0.6) \times 10^{-4}$ for events with both vertices reconstructed with more than one track, and $(3.1 \pm 0.1) \times 10^{-2}$ for events with at least one single-track vertex.

After flavor tagging and vertexing, we find 5417 events in total in the signal region, which are used for the $\sin 2\phi_1$ determination. Table II lists the numbers of candidates, $N_{\text{ev}}$, and the estimated signal purity for each $f_{CP}$ mode. Figure I shows the $M_{\text{bc}}$ distribution after applying mode-dependent requirements on $\Delta E$ for all $B^0$ candidates except for $B^0 \rightarrow J/\psi K^0_L$. There are 3085 entries in total in the signal region defined as $5.27 < M_{\text{bc}} < 5.29$ GeV/$c^2$. Figure II shows the $p_B^{\text{CMS}}$ distribution for $B^0 \rightarrow J/\psi K^0_L$ candidates. We find 2332 entries in the $0.20 \leq p_B^{\text{CMS}} \leq 0.45$ GeV/$c$ signal region.

Figure III shows the observed $\Delta t$ distributions for the $q\xi_f = +1$ and $q\xi_f = -1$ event samples (top), the asymmetry between two samples with $0 < r \leq 0.5$ (middle) and with $0.5 < r \leq 1.0$ (bottom). The asymmetry in the region $0.5 < r \leq 1.0$, where wrong-tag fractions are small as shown in Table II, clearly demonstrates large $CP$ violation.

We determine $\sin 2\phi_1$ from an unbinned maximum-likelihood fit to the observed $\Delta t$ distributions. The probability density function (PDF) expected for the signal distribution is given by

$$P_{\text{sig}}(\Delta t, q, w_l, \Delta w_l, \xi_f) = \frac{e^{-|\Delta t|/\tau_{B^0}}}{4\tau_{B^0}}[1 - q\Delta w_l - q\xi_f(1 - 2w_l)\sin 2\phi_1 \sin(\Delta m_d\Delta t)],$$

where we fix the $B^0$ lifetime $\tau_{B^0}$ and mass difference $\Delta m_d$ at their world average values. Each PDF is convolved with the appropriate $R_{\text{sig}}(\Delta t)$ to determine the likelihood value for
TABLE II: The numbers of reconstructed $B \to f_{CP}$ candidates after flavor tagging and vertex reconstruction, $N_{\text{ev}}$, and the estimated signal purity, $p$, in the signal region for each $f_{CP}$ mode. $J/\psi$ mesons are reconstructed in $J/\psi \to \mu^+\mu^-$ or $e^+e^-$ decays. Candidate $K_S^0$ mesons are reconstructed in $K_S^0 \rightarrow \pi^+\pi^-$ decays unless otherwise written explicitly.

| Mode                                      | $\xi_f$ | $N_{\text{ev}}$ | $p$       |
|-------------------------------------------|---------|-----------------|-----------|
| $J/\psi K_S^0$                            | -1      | 1997            | 0.976 ± 0.001 |
| $J/\psi K_S^0(\pi^0\pi^0)$               | -1      | 288             | 0.82 ± 0.02  |
| $\psi(2S)(\ell^+\ell^-)K_S^0$            | -1      | 145             | 0.93 ± 0.01  |
| $\psi(2S)(J/\psi\pi^+\pi^-)K_S^0$        | -1      | 163             | 0.88 ± 0.01  |
| $\chi_{c1}(J/\psi\gamma)K_S^0$          | -1      | 101             | 0.92 ± 0.01  |
| $\eta_c(K_S^0K^-\pi^+)$                  | -1      | 123             | 0.72 ± 0.03  |
| $\eta_c(K^+K^-\pi^0)$                    | -1      | 74              | 0.70 ± 0.04  |
| $\eta_c(p\bar{p})K_S^0$                  | -1      | 20              | 0.91 ± 0.02  |
| All with $\xi_f = -1$                     | -1      | 2911            | 0.933 ± 0.002 |
| $J/\psi K^{*0}(K_S^0\pi^0)$              | +1(81%) | 174             | 0.93 ± 0.01  |
| $J/\psi K_L^0$                            | +1      | 2332            | 0.60 ± 0.03  |

FIG. 1: The beam-energy constrained mass distribution within the $\Delta E$ signal region for all $f_{CP}$ modes other than $J/\psi K_L^0$. The solid curve shows the fit to signal plus background distributions, and the dashed curve shows the background contribution.
FIG. 2: The $p_B^{\text{cms}}$ distribution for $B^0 \rightarrow J/\psi K^0_L$ candidates with the results of the fit. The dashed lines indicate the signal region ($0.20 \leq p_B^{\text{cms}} \leq 0.45$ GeV/c).

each event as a function of $\sin 2\phi_1$:

$$P_i = (1 - f_{\text{ol}}) \int \left[ f_{\text{sig}} P_{\text{sig}}(\Delta t', q, w_1, \Delta w_l, \xi_f) R_{\text{sig}}(\Delta t - \Delta t') 
+ (1 - f_{\text{sig}}) P_{\text{bkg}}(\Delta t') R_{\text{bkg}}(\Delta t - \Delta t') \right] d\Delta t' + f_{\text{ol}} P_{\text{ol}}(\Delta t),$$

(3)

where $f_{\text{sig}}$ is the signal fraction calculated as a function of $p_B^{\text{cms}}$ for $J/\psi K^0_L$ and of $\Delta E$ and $M_{Bc}$ for other modes. $P_{\text{bkg}}(\Delta t)$ is the PDF for combinatorial background events, which is modeled as a sum of exponential and prompt components. It is convolved with a sum of two Gaussians, $R_{\text{bkg}}$, which is regarded as a resolution function for the background. To account for a small number of events that give large $\Delta t$ in both the signal and background, we introduce the PDF of the outlier component, $P_{\text{ol}}$, and its fraction $f_{\text{ol}}$. The only free parameter in the final fit is $\sin 2\phi_1$, which is determined by maximizing the likelihood function $L = \prod_i P_i$, where the product is over all events. The result of the fit is

$$\sin 2\phi_1 = 0.733 \pm 0.057(\text{stat}) \pm 0.028(\text{syst}).$$

Sources of systematic error include uncertainties in the flavor tagging (0.014), in the vertex reconstruction (0.013), in the background fractions for $B^0 \rightarrow J/\psi K^0_L$ (0.012) and for other modes (0.007), in the resolution function (0.008), a possible bias in the $\sin 2\phi_1$ fit (0.008), and an effect of interferences [12] in the $f_{\text{tag}}$ final state (0.008). The errors introduced by uncertainties in $\Delta m_d$, $\tau_{B^0}$ and in the background $\Delta t$ distribution, are less than 0.005.

Several checks on the measurement are performed. Table III lists the results obtained by applying the same analysis to various subsamples. All values are statistically consistent with
FIG. 3: The $\Delta t$ distributions for the events with $q_{\xi_f} = -1$ (open points) and $q_{\xi_f} = +1$ (solid points) with all modes combined (top), the asymmetry in each $\Delta t$ bin between $q_{\xi_f} = -1$ and $q_{\xi_f} = +1$ samples with $0 < r \leq 0.5$ (middle), and with $0.5 < r \leq 1$ (bottom). The results of the global unbinned maximum-likelihood fit ($\sin 2\phi_1 = 0.733$) are also shown.

each other. Figure 4 shows the raw asymmetries and the fit results for $(c\bar{c})K^0_S$ (top) and $J/\psi K^0_L$ (bottom). A fit to the non-$CP$ eigenstate modes $B^0 \rightarrow D^{*-} \ell^+ \nu$ and $J/\psi K^{*0}(K^+\pi^-)$, where no asymmetry is expected, yields $0.012 \pm 0.013$(stat).

The signal PDF for a neutral $B$ meson decaying into a $CP$ eigenstate [Eq. (2)] can be expressed in a more general form as

$$
P_{\text{sig}}(\Delta t, q, w_l, \Delta w_l) = e^{-|\Delta t|/\tau_B^0} \left\{ 1 - q\Delta w_l + q(1 - 2w_l) \left[ S \sin(\Delta m_d \Delta t) + A \cos(\Delta m_d \Delta t) \right] \right\},$$

where $S \equiv 2\Im(\lambda)/(|\lambda|^2 + 1)$, $A \equiv (|\lambda|^2 - 1)/(|\lambda|^2 + 1)$, and $\lambda$ is a complex parameter that depends on both $B^0$-$\bar{B}^0$ mixing and on the amplitudes for $B^0$ and $\bar{B}^0$ decay to a $CP$
TABLE III: The numbers of candidate events, \( N_{\text{ev}} \), and values of \( \sin 2\phi_1 \) for various subsamples (statistical errors only).

| Sample                      | \( N_{\text{ev}} \) | \( \sin 2\phi_1 \) |
|-----------------------------|----------------------|---------------------|
| \( J/\psi K^0_S(\pi^+\pi^-) \) | 1997                 | 0.67 ± 0.08         |
| \( J/\psi K^0_S(\pi^0\pi^0) \) | 288                  | 0.72 ± 0.20         |
| \( \psi(2S)K^0_S \)          | 308                  | 0.89 ± 0.20         |
| \( \chi_{c1} K^0_S \)        | 101                  | 1.54 ± 0.49         |
| \( \eta_c K^0_S \)           | 217                  | 1.32 ± 0.29         |
| All with \( \xi_f = -1 \)    | 2911                 | 0.73 ± 0.06         |
| \( J/\psi K^0_L \)           | 2332                 | 0.80 ± 0.13         |
| \( J/\psi K^{*0}(K^0_S\pi^0) \) | 174                  | 0.10 ± 0.45         |
| \( f_{\text{tag}} = B^0 (q = +1) \) | 2717                 | 0.72 ± 0.09         |
| \( f_{\text{tag}} = \bar{B}^0 (q = -1) \) | 2700                 | 0.74 ± 0.08         |
| \( 0 < r \leq 0.5 \)         | 2985                 | 0.95 ± 0.26         |
| \( 0.5 < r \leq 0.75 \)      | 1224                 | 0.68 ± 0.11         |
| \( 0.75 < r \leq 1 \)        | 1208                 | 0.74 ± 0.07         |
| data set I (78 fb\(^{-1}\))  | 3013                 | 0.73 ± 0.07         |
| data set II (62 fb\(^{-1}\)) | 2404                 | 0.74 ± 0.09         |
| All                         | 5417                 | 0.733 ± 0.057       |

FIG. 4: The raw asymmetries for \((c\bar{c})K^0_S (\xi_f = -1)\) (top) and \(J/\psi K^0_L (\xi_f = +1)\) (bottom). The curves are the results of the global unbinned maximum-likelihood fit.
eigenstate. The presence of the cosine term ($|\lambda| \neq 1$) would indicate direct $CP$ violation; the value for $\sin 2\phi_1$ reported above is determined with the assumption $|\lambda| = 1$, as $|\lambda|$ is expected to be very close to one in the SM. In order to test this assumption, we also performed a fit using the expression above with $a_{CP} \equiv -\xi_f \text{Im} \lambda/|\lambda|$ and $|\lambda|$ as free parameters, keeping everything else the same. We obtain

$$|\lambda| = 1.007 \pm 0.041\,\text{(stat)},$$
$$a_{CP} = 0.733 \pm 0.057\,\text{(stat)},$$

for all $CP$ modes combined. This result is consistent with the assumption used in our analysis.

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[1] M. Kobayashi and T. Maskawa, Prog. Theor. Phys. 49, 652 (1973).
[2] A. B. Carter and A. I. Sanda, Phys. Rev. D 23, 1567 (1981); I. I. Bigi and A. I. Sanda, Nucl. Phys. B193, 85 (1981).
[3] Belle Collaboration, K. Abe et al., Phys. Rev. Lett. 87, 091802 (2001); Phys. Rev. D 66, 032007 (2002).
[4] Belle Collaboration, K. Abe et al., Phys. Rev. D 66, 071102 (2002).
[5] BaBar Collaboration, B. Aubert et al., Phys. Rev. Lett. 87, 091801 (2001); Phys. Rev. D 66, 032003 (2002); Phys. Rev. Lett. 89, 201802 (2002).
[6] Belle Collaboration, A. Abashian et al., Nucl. Instrum. Methods Phys. Res. A 479, 117 (2002).
[7] S. Kurokawa and E. Kikutani et al., Nucl. Instrum. Methods A 499, 1 (2003).
[8] Throughout this paper, when a decay mode is quoted, the inclusion of the charge conjugate mode is implied.
[9] Belle Collaboration, K. Abe et al., Phys. Lett. B 538, 11 (2002).
[10] H. Tajima et al., hep-ex/0301026
[11] Particle Data Group, K. Hagiwara et al., Particle Listings in the 2003 Review of Particle Physics, http://www-pdg.lbl.gov/2003/contents_listings.html
[12] O. Long, M. Baak, R. N. Cahn and D. Kirkby, hep-ex/0303030