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Lambda hyperon production and polarization in collisions of p (3.5 GeV) + Nb

HADES collaboration

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Abstract. Results on Λ hyperon production are reported for collisions of p (3.5 GeV) + Nb, studied with the High Acceptance Di-Electron Spectrometer (HADES) at SIS18 at GSI Helmholtzzentrum for Heavy-Ion Research, Darmstadt. The transverse mass distributions in rapidity bins are well described by Boltzmann shapes with a maximum inverse slope parameter of about 90 MeV at a rapidity of y = 1.0, i.e. slightly below the center-of-mass rapidity for nucleon-nucleon collisions, y_{cm} = 1.12. The rapidity density decreases monotonically with increasing rapidity within a rapidity window ranging from 0.3 to 1.3. The Λ phase-space distribution is compared with results of other experiments and with predictions of two transport approaches which are available publicly. None of the present versions of the employed models is able to fully reproduce the experimental distributions, i.e. in absolute yield and in shape. Presumably, this finding results from an insufficient modelling in the transport models of the elementary processes being relevant for Λ production, rescattering and absorption. The present high-statistics data allow for a genuine two-dimensional investigation as a function of phase space of the self-analyzing Λ polarization in the weak decay Λ → pπ−. Finite negative values of the polarization in the order of 5 – 20 % are observed over the entire phase space studied. The absolute value of the polarization increases almost linearly with increasing transverse momentum for p_{T} > 300 MeV/c and increases with decreasing rapidity for y < 0.8.

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1 Introduction

During the past two decades strangeness carrying particles which are produced in relativistic heavy-ion reactions at energies around the corresponding production thresholds in nucleon-nucleon (NN) collisions attracted strong attention from both experimental and theoretical sides [1,2,3,4,5]. Since their production and propagation are expected to provide insight into the nature of hot and dense nuclear matter. For instance, at energies available at SIS18/GSI Darmstadt densities up to three times that of ground-state nuclear matter and temperatures up to ∼100 MeV can be achieved. In the pioneering work of the KaoS collaboration at SIS18 on sub-threshold kaon production [6] and based on comparisons to transport approaches [7,8] a soft equation of state (EoS) was extracted as predicted already before [9,10]. A strong focus was put on the study of in-medium properties of kaons and antikaons. Especially, their collective flow and spectral shapes at low transverse momenta are expected to be altered within the nuclear environment. The corresponding nuclear mean-field potential acting on the kaons and antikaons are predicted to be weakly positive (∼20 to 40 MeV) and strongly negative (∼−50 to −80 MeV), respectively [11,12]. Kaon and antikaon phase-space distributions [13,14,15,16,17,18] as well as azimuthal emission (flow) patterns of kaons [19,20,21] support these predictions while the antikaon flow data are not conclusive yet. The tight interplay of experimental and and theoretical efforts revealed the importance of strangeness-exchange reactions for antikaon production (YN → KNN) and absorption (KN → Y π). Also Λ hyperons, being co-produced with kaons, are predicted to feel a weakly attractive potential (∼−30 MeV) [22,23,24]. However, experimental data on the flow properties [25] and on spectral shapes [15,26,27] of hyperons produced in heavy-ion collisions near or below threshold are scarce. Evidently, not only nucleus-nucleus but also nucleon-nucleon collisions, though proceeding at densities not exceeding nuclear-matter ground-state density, may contribute to the discussion on medium modifications of meson and baryon properties. Here, valuable information has been collected by the KaoS collaboration, too [28]. The availability of such information is of great importance, since the reliable characterization of strangeness production and propagation in pA collisions is an indispensable prerequisite for the understanding of heavy-ion collisions. No experimental information is available on hyperon production in case of near-threshold nucleon-nucleus collisions which is assumed to serve as a link between elementary NN and heavy-ion collisions. Such data would allow for an improvement of the predictive power on the strangeness sector of state-of-the-art transport approaches which partially lack reliable input information on elementary processes.

Parity conservation in strong interaction requires that the spin of produced Λ hyperons is aligned perpendicularly to the production plane. In the parity-nonconserving weak process, $\Lambda \rightarrow pt^{-}$, the Λ polarization causes a significant up-down asymmetry of the decay proton w.r.t. that plane. The Λ polarization, surprisingly appearing in inclusive reactions with unpolarized beams and targets, was first observed in 1976 at Fermilab in collisions of p(300 GeV) + Be [29]. The observation of the negative polarization and the strong (almost linear) transverse-momentum dependence of its magnitude was rapidly confirmed in p(24 GeV/c) + Pt collisions at CERN-PS [30], in p(400 GeV) + Be again at the Fermilab neutral hyperon beam (Λ and $\bar{\Lambda}$) [31], in p(28.5 GeV/c) + Ir at AGS [26], and in p(12 GeV) + W at KEK [33]. Λ polarization measurements in pp interactions at the CERN intersecting storage rings [34] showed no obvious dependence on $\sqrt{s}$ which was varied from 31 to 62 GeV (which would correspond to 510 and 2050 GeV beam protons on a stationary proton target). However, the polarization was found to increase strongly with Feynman-$x$ ($x_F$) and with transverse momentum approaching -40% when both quantities are maximum. Experiments with polarized beams followed soon, e.g. p + Be collisions at 13.3 and 18.5 GeV/c at the AGS [35]. It is worth mentioning that all of these early experiments consisted of magnetic spectrometers set to fixed scattering angles. But more importantly, they suffered from a rather small solid-angle coverage resulting in a high degree of correlation between the transverse ($p_t$) and longitudinal ($x_F$ or rapidity) coordinates (e.g. in pN reactions at 450 GeV at CERN-SPS [36]). Any larger phase-space coverage implied a time-consuming setting of the corresponding spectrometer to different scattering angles with proper relative normalization as tried at Fermilab in p(400 GeV) collisions on Be, Cu, and Pb targets with the main focus on the behaviour of the Λ and $\bar{\Lambda}$ polarization at large transverse momentum [37]. The first exclusive measurements of the Λ polarization were performed with the E766 experiment at the AGS at $p_{p+p} \rightarrow K^+ (\pi^- \pi^-)^n (n=1-4)$ at 27.5 GeV/c [38,39]. Λ polarization in pp collisions is antisymmetric in $x_F$ by virtue of rotational invariance. Since the detector used had uniform acceptance in $x_F$, the same polarization magnitude was measured for positive and negative $x_F$. The behaviour of the polarization in $x_F$ and $p_t$ was found the same for all of the studied reactions. First polarization studies of Λ hyperons produced in heavy-ion collisions (10.7 GeV Au + Au) were reported by the EB96 collaboration at BNL-AGS [40]. Their results revealed a dependence of the polarization on the transverse momentum and $x_F$ being consistent with previous measurements in pp and pA collisions. The polarization of Λ hyperons produced inclusively by a $\Sigma^-$ beam of 340 GeV/c at CERN-SPS [41], however, exhibited the striking feature of the mostly positive sign of the polarization which is opposite to what has been observed in Λ production by protons or neutrons. The HERMES collaboration at DESY determined Λ and $\bar{\Lambda}$ polarizations in quasi-elastic photoproduction at the 27.6 GeV positron beam of the HERA collider on an internal gas target [42]. Surprisingly, the Λ polarization, averaged over the acceptance of the spectrometer, appeared positive, in contrast to almost all other experiments, while the $\bar{\Lambda}$ polarization appeared compatible with zero. A linear rise of the Λ polarization magnitude with increasing transverse momentum was found similar to that observed in earlier experiments.

At lower beam energies only few hyperon polarization data exist. The DISTO collaboration at SATURNE investigated strangeness production in elementary pp collisions with polarized proton beam at 3.67 GeV/c [43]. First polarization transfer measurements for exclusive hyperon production reactions were reported in ref. [44]. At COSY, the TOF collaboration studied Λ polarization in the elementary $pp \rightarrow pK^+\Lambda$ reaction with polarized beams at 2.75 and 2.95 GeV/c [45,46,47]. At higher energies around the corresponding production}
energy and similar to DISTO [43] and E766 at AGS [38], the experiments revealed a negative (positive) polarization in the beam (target) fragmentation region, while the polarization seemed to vanish at the lower energy. Besides the polarization of the Λ hyperon, the Λ analyzing power and the spin-transfer coefficient, also referred to as Λ depolarization, could be determined. The lowest beam energy so far for which a Λ polarization value could be determined amounts to 1.8 GeV. For central-nucleus-nucleus collisions of Ar+KCl at this beam kinetic energy per incident nucleon, the streamer-chamber group at the BEVALAC reported an average Λ polarization value of about \(-0.10 \pm 0.05\) [49]. For recent reviews including parameterizations of various polarization dependences on kinematic quantities we refer the reader to refs. [49] [50] [51].

While the Λ polarization seems to be established as an experimental fact, its origin remains a mystery. Various models are proposed, assigned either to the quark-exchange [52,53,54,55,56,57] or to the meson-exchange picture [58,59,60,61,62]. But, there is still no theoretical description which is able to explain the experimental observations consistently [49].

Summarizing the experimental situation on Λ production and polarization, we conclude that the high-acceptance spectrometer HADES [63] would be an appropriate experimental device allowing for I) the investigation of the Λ phase-space distribution in proton-nucleus collisions and II) the study of a genuine two-dimensional (transverse, longitudinal) dependence of the Λ polarization over a large phase-space region, feasible with one and the same apparatus setting.

The present paper is organized as follows. In Sect. 2 we give an overview of the HADES experiment on p + Nb collisions at 3.5 GeV beam kinetic energy. We proceed with the data analysis in Sect. 3. In Sect. 3.1 we present the method to identify the Λ hyperons from their weak decay into proton-π− pairs, while in Sect. 3.2 we describe the analysis chain for the extraction of experimental Λ phase-space distributions and the corresponding predictions by transport models. In Sect. 3.3 the results on the Λ polarization and its phase-space dependence will be presented. Finally, in Sect. 4 we summarize our results.

2 The experiment

The experiment was performed with the High Acceptance Di-Electron Spectrometer (HADES) at the Schwerionen-synchrotron SIS18 at GSI, Darmstadt. HADES, although primarily optimized to measure di-electrons [64], offers excellent hadron identification capabilities [18,27,65,66,67] allowing for a profound correlation analysis. A detailed description of the spectrometer is presented in ref. [63]. The present results are based on a dataset which was previously analyzed with respect to e+e− [68] as well as to pion and η production [69,70] in collisions of p + Nb at 3.5 GeV; the production of K0 mesons, focusing on the K0 phase-space distribution and its alteration due to the influence of a kaon-nucleon potential at nuclear-matter ground-state density, will be reported elsewhere. In the following we summarize the main features of the apparatus.

HADES consists of a 6-coil toroidal magnet centered on the beam axis and six identical detection sections located between the coils and covering polar angles from 18 to 85 degrees. The six sectors consist of hadron blind Ring-Imaging Cherenkov (RICH) detectors (not used for the present investigation), four planes of Multi-wire Drift Chambers (MDCs) for track reconstruction, and two time-of-flight walls. TOFino (polarg angles 18° < θ < 44°) and TOF (44° < θ < 85°), supplemented at forward polar angles with Pre-Shower chambers. The TOF and TOFino+Pre-Shower detectors were combined into a Multiplicity and Electron Trigger Array (META). A reconstructed track in the spectrometer is composed of straight inner and outer track segments in the MDCs. The pointing vector of the outer track segment is used for matching with a META hit. Possible trajectories through pairs of inner and outer track segments are combined to track candidates. A Runge-Kutta algorithm allows to calculate the moment of each track candidate making use of the track deflection in the magnetic field between the inner and outer segments. The quality of the META-hit matching and the Runge-Kutta fitting (characterized by χ2 values) is used to create an ordered list of track candidates. The track candidate with the lowest product of both χ2 values is selected as the true track. Its segments and associated track candidates are then deleted from the candidate list. This procedure is repeated until no track candidates are left in the list.

Particle identification of protons and π− mesons is based on the correlation of their momenta and energy loss in the MDCs. Two-dimensional cuts in the corresponding correlation plots are used to select the different particle species. For more details, e.g. the quality of kaon identification, see refs. [65,66]. Finally, the momentum calculated from the track curvature is corrected for the energy loss of the charged particles in the target, beam pipe and detector materials.

In the present experiment, a proton beam of about 2 × 106 particles per second with kinetic energy of 3.5 GeV (corresponding to an excess energy w.r.t. the threshold for Λ production in NN collisions of $\sqrt{s_{NN}} - \sqrt{s_{NN,A}} = 0.63$ GeV) was incident on a 12-fold segmented target of natural niobium (50Nb). The choice of the target was the result of simulations aimed at optimizing the di-electron experiment [68], i.e. compromising on the ratio of the vector-meson production and the combinatorial background due to γ conversion. However, the usage of this medium-size target is of advantage also for the present Λ investigations, since the p−π− combinational background increases stronger with target mass than the Λ yield which in turn is tightly connected to the production of the associated kaons [28]. The data readout was started by different trigger decisions [69]. For the present analysis, we employ only the data of the first-level trigger (LVL1, down-scaled by a factor of three), requiring a charged-particle multiplicity $\geq 3$ in the TOF/TOFino detectors. We processed about $N_{ev} = 3.2 \times 10^9$ of such LVL1 events. The total reaction cross section of $\sigma_{p,Nb} = (848 \pm 127)$ nb is provided by measuring charged pions and by interpolating known pion production cross sections [68,70].

3 Analysis

3.1 Λ identification

It is important to mention that Σ0 hyperons decay almost exclusively into Λ’s via the decay $\Sigma^0 \rightarrow \Lambda \gamma$ (branching ratio $BR = 100\%$, lifetime $\tau = 2.22 \times 10^{-11}$ m [71]), with the...
of age, lower momenta and hence tracks with higher curvature. A corresponding widths measured in previous HADES analyses. It amounts to 3.1 MeV as the weighted average of the sigma widths of both Gaussians.

1115 Gaussian fit to the peak, the pole mass is determined to be the limit, i.e. the sum of the proton and the data near (1.085 GeV) + KCl [27,67] where, on average, -1/3 the polarization of the \( \Sigma^0 \) [30]. The latter one is predicted and measured [72] to be opposite to that of the \( \Lambda \).

In the present analysis, we identify the \( \Lambda \) hyperons through their weak decay \( \Lambda \rightarrow p\pi^- \) (\( BR = 63.9\%, c\tau = 7.89 \text{ cm} \)), with the charged daughter particles detected in HADES [27,67]. The long lifetime of the \( \Lambda \) causes a sizeable fraction of these particles to decay away from the primary vertex. The precision of the track reconstruction with HADES is sufficient to resolve these secondary vertices [65,67]. For the selection of \( \Lambda \)'s, topological cuts are used. As a compromise between a high \( \Lambda \) yield and a reasonable signal-to-background ratio (> 0.1 all over the investigated phase space), we choose

i) a minimum value of the \( \Lambda \) decay vertex distance to the primary vertex, \( d_V > 43 \text{ mm} \),

ii) minimum values of the proton and \( \pi^- \) shortest track distances to the primary vertex, \( d_p > 4 \text{ mm}, d_{\pi^-} > 10 \text{ mm} \), and

iii) an upper threshold of the proton-\( \pi^- \) minimum track distance, \( d_{\pi^-} < 10 \text{ mm} \).

Here, the off-vertex cut i) is the main condition responsible for the extraction of a \( \Lambda \) signal with good (\( \sim 1 \)) signal-to-background ratio. Figure 1 shows the invariant-mass distribution of all proton-\( \pi^- \) pairs which pass the cuts listed above. To extract the \( \Lambda \) yield, the invariant-mass spectrum is fitted, typically in the range from 1090 to 1200 MeV, with a combination of different functions describing both the signal and the combinatorial background of uncorrelated proton-\( \pi^- \) pairs. The signal peak is parametrized by two Gaussians (with identical mean values but different widths to account for a certain broadening of the peak at its base), while the background is approximated by a Tsallis (q-exponential) function, \( f_T(x) \propto (1 - (1 - q)x)^{1/(1 - q)} \). Here, \( x \) is a linear function of the invariant mass, \( m_{p\pi^-} \), and \( q \) is a shape parameter which may account for the phase-space limitation at large invariant masses, due to energy-momentum conservation. (Approximating instead the combinatorial background with the event-mixing technique, a quite similar quality of reproduction of the invariant-mass distribution over almost the entire mass ranges below and above the peak (\( (m_{p\pi^-} - m_{\Lambda}) > 4\sigma_{\Lambda} \)) is possible, with a slight exception of some underestimate of the data near (\( m_{p\pi^-} < 1085 \text{ MeV}/c^2 \)) to the kinematical limit, i.e. the sum of the proton and \( \pi^- \) masses.) From the Gaussian fit to the peak, the pole mass is determined to be \( 1115.6 \pm 0.1 \text{ MeV}/c^2 \), in very good agreement with the value of \( 1115.863 \pm 0.006 \text{ MeV}/c^2 \) listed by the Particle Data Group [71]. The peak width, which is a pure apparatus effect, is taken as the weighted average of the sigma widths of both Gaussians. It amounts to \( 3.1 \text{ MeV}/c^2 \), being only slightly larger than the corresponding widths measured in previous HADES analyses of the system Ar (1.76 A GeV) + KCl [27,67] where, on average, lower momenta and hence tracks with higher curvature are involved. In total, for the cuts listed above and after background subtraction, about \( 1.1 \times 10^6 \) \( \Lambda \) hyperons were reconstructed within a \( \pm 2\sigma \) window around the peak mass, with a mean signal-to-background ratio of 1.1.

![Figure 1](image.png)

**Figure 1.** Proton-\( \pi^- \) invariant mass distribution (symbols) with the \( \Lambda \) signal peak in the reaction p (3.5 GeV) + Nb. The full curve shows the result of a common fit with two Gaussians for the peak and a Tsallis function for the background (see text). The dashed curve represents the background. The vertical dotted lines bound the \( 2\sigma \) window for signal counting.

### 3.2 \( \Lambda \) inclusive phase-space distribution

#### 3.2.1 Experimental data

The bottom right panel of Fig. 2 shows the two-dimensional raw data yield (i.e. \( \Lambda \) peak yields extracted from the proton-\( \pi^- \) invariant-mass distributions after subtraction of the combinatorial background) as a function of transverse momentum and rapidity. Corrections for detector acceptance and reconstruction efficiency were performed with Monte-Carlo simulations involving, as appropriate event generator, the UrQMD transport approach [23,24] and the GEANT [25] package accounting for the proper particle decays and the finite detector acceptance, granularity, resolution, etc. The minor missing experimental yield outside the \( 2\sigma \) window around the \( \Lambda \)-peak mass (cf. Fig. 1) is well considered by applying the same cut to the simulation which exhibits a similar broadened peak base proved to be due to small-angle scattering in air and in the detector materials of the \( \Lambda \) decay products. The bottom left panel of Fig. 2 displays the GEANT output, while the middle left panel shows the UrQMD output. The ratio of both distributions of simulated \( \Lambda \) data delivers the corresponding reconstruction efficiency matrix (top left panel). Note that also the
bias on the $\Lambda$ yield due to the effect of the LVL1 trigger is estimated with the help of UrQMD+GEANT simulations. An enhancement of the LVL1 triggered yield over the minimum-bias value of $1.53 \pm 0.02$ has been found which is corrected for when determining the final (minimum-bias) $\Lambda$ yield as a function of phase-space population. Within the given marginal uncertainty, the correction factor itself exhibits no dependence on phase space. Finally, after dividing – for each phase-space cell – the experimental raw data by the corresponding efficiency, the distribution corrected for acceptance, reconstruction efficiency, LVL1 trigger bias, and non-target interaction ($\approx 17\%$ events w/o tracks), is derived and displayed in the middle right panel of Fig. 2. Note that this phase-space distribution is the prerequisite for the two-dimensional investigation of the $\Lambda$ polarization presented in Sect. 3.3.

To extrapolate into the unmeasured region at low transverse momentum, we follow the widely applicable and commonly used recipe of approximating the $p_t$ spectra by Maxwell-Boltzmann distributions. To do so, we start with the triple differential yield $d^3N/dp_t dy \propto \exp\left(-E/T\right)$. Here, $E = ((p_t/c)^2 + (m_0c^2)^2)^{1/2} = m_t c^2 \cosh y$ is the total energy, $y = \tanh^{-1}(p_t/E/c)$ is the lab. rapidity, $m_t = ((p_t/c)^2 + m_0^2)^{1/2}$ is the transverse mass, $p_t$ ($p_\parallel$) is the transverse (longitudinal in beam direction) momentum, and $m_0$ is the rest mass of the particle of interest. Finally, $c$ gives the speed of light in vacuum. Transformation from spherical to cylindrical coordinates (being more appropriate for an almost rotational symmetric apparatus) and integration over the azimuthal angle delivers the two-dimensional yield

$$\frac{d^2N}{m_t^2 dm_t dy} = C_B(y) \exp\left(-\frac{m_t c^2}{T_B(y)}\right).$$

(1)

Fits with a simple exponential to these transverse-mass spectra in slices of rapidity deliver constants, $C_B(y)$, and inverse (Boltzmann) slope parameters, $T_B(y)$. Figure 3 shows the $m_t$ distributions for the indicated rapidity regions. The lines are Boltzmann fits to the data according to Eq. (1). For the determination of the $dN/dy$ distribution, the experimental data, where available, are integrated, and the yield in the unmeasured region is obtained from the fit.

![Fig. 2. Bottom right: Raw $\Lambda$ yield $d^2N/dp_t dy$. Bottom left: GEANT output of UrQMD simulations. Middle left: GEANT input (UrQMD output). Top left: Reconstruction efficiency matrix as derived from the ratio of the distributions below. Middle right: Experimental $\Lambda$ yield after correction with the efficiency matrix.](image1)

![Fig. 3. Experimental $\Lambda$ yield distribution $m_t^{-2}d^2N/dm_t dm_t$ (symbols with error bars) in slices of rapidity as given in the legend. The lines represent fits with an exponential distribution according to Eq. (1). Full lines cover the corresponding fit regions. Extended dashed lines display the part used for extrapolation.](image2)

Before we present the rapidity dependences of the inverse slope parameter, $T_B(y)$, and the rapidity density distribution, $dN/dy$, of $\Lambda$ hyperons produced in $p$+Nb collisions, we show the result of a self-consistency check, i.e. using UrQMD simulations for the acceptance and reconstruction efficiency corrections and analyzing another simulation similarly to the experimental data. For this purpose, we used the fireball option of the event generator Pluto [76]. Based on the expected experimental phase-space distribution, we generated $\Lambda$ hyperon...
events populating the phase space according to an isotropic thermal source with a temperature of $T = 50$ MeV centered at an average rapidity of $\langle y \rangle = 0.56$. The Pluto events were tracked through GEANT to account for the detector response and the geometrical decay topology. The GEANT output was embedded into experimental events to account for a proper track environment and, finally, passed through the entire analysis chain with the correction matrix taken from UrQMD simulation. Figure 4 shows the result for the rapidity distribution. Though the shapes of both simulations differ significantly, the initial shape of the phase-space distribution generated by Pluto is well recovered. Hence, we are convinced that our reconstruction method is based on solid grounds. Furthermore, we note that the experimental distributions given below represent the average of two analyses from two independent groups [77,78]. The given systematic errors comprise the slight differences of the corresponding analysis results and those from a variation of the cut values given in Sect. 3.1 within reasonable limits ($\pm 20\%$). The statistical errors are often smaller than the symbols displayed in the figures.

Figure 5 presents the dependence of the $\Lambda$ inverse (Boltzmann) slope parameter, $T_B(y)$, (symbols) as derived from the exponential fits in Fig. 3. The error bars represent the systematic errors. The full and dashed curves display similar dependences resulting from corresponding fits to the spectra of the transport approaches UrQMD and GiBUU, respectively. The dotted curve represents the function $T_B(y) = 92$ MeV/$\cosh(y - 1.0)$. The arrow indicates the center-of-mass rapidity in nucleon-nucleon collisions at 3.5 GeV.
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Integrating the two-dimensional phase-space distribution over transverse momentum, the $\Lambda$ rapidity-density distribution, $dN/dy$, is derived. It is displayed in Fig. 6. Except for the first data point, the statistical errors are smaller than the symbols. The given error bars represent the systematic errors. The gray-shaded band displays the uncertainty of the absolute normalization of about 12%. In contrast to symmetric heavy-ion collisions at comparable beam energies, where the rapidity distributions of secondary particles are symmetric around maxima at the center-of-mass rapidity of the nucleon-nucleon system \cite{15, 26, 27, 77, 80, 81}, the present $\Lambda$ yield at rapidities of $y > 0.3$ decreases monotonically with increasing rapidity. Unfortunately, the interesting region around target rapidity is not covered by the detector, due to its limiting upper polar angle, $\theta < 85$ degrees. For comparison, we note that our pion and $\eta$ meson analyses in the same collision system, p (3.5 GeV) + Nb, showed Gaussian shaped rapidity distribution centered, however, at rapidities of about 0.95 \cite{82}, i.e. well below $y_{cm}$. Even slower emission sources ($\beta \approx 0.5 - 0.6$) are estimated by KaoS for $K^+$ and $K^-$ production in p+Au collisions at 3.5 GeV \cite{28}. It is worth to be noted that this observation is confirmed by our preliminary data on $K^0$ meson production in p+Nb exhibiting a rapidity density distribution centered around $y \approx 0.6$ \cite{82}.

3.2.2 Comparison with other data

Looking for other experimental results on $\Lambda$ production in pA collisions, no data could be found at beam energies below 9 GeV. The results next to ours are derived with the JINR Dubna 2 m propane bubble chamber for collisions of p+C at 10 GeV/c \cite{83, 84}, i.e. already at an excess energy w.r.t. the $\Lambda$ threshold in NN collisions of $\sqrt{s_{NN}} = 2$ GeV. The authors report a $\Lambda$ production probability of (0.053 ± 0.005). The transverse momentum spectrum was found slightly harder than ours, as expected from the higher beam energy allowing for more energetic particles and hence larger transverse momenta. The rapidity distribution appeared asymmetric with the upper tail reaching to rapidities of 2.6. The maximum and mean values are located at about 0.8 and 1.0, respectively, i.e. both are well below the corresponding c.m. rapidity for NN collisions ($y_{cm} = 1.53$), qualitatively similar to our observation (Fig. 5). Similar results have already been reported earlier in central collisions of carbon and oxygen at 4.5 GeV/c beam momentum per incident nucleon on different target nuclei, as measured with the 2 m streamer chamber SKM-200 at the Synchrophasotron in Dubna \cite{85, 86}. Systematically increasing the target mass, the authors found a $\Lambda$ rapidity distribution which steadily became asymmetric and shifted towards target rapidity.

To be able to compare our $\Lambda$ production probability to the strange particle yields of another proton-nucleus experiment performed at the same beam energy but with different target nuclei, i.e. KaoS data on $K^+$ and $K^-$ production in p+C and p+Au collisions \cite{88}, we normalize the yields to the number of participants, $A_{part}$. Using a nuclear overlap (Glauber) model \cite{87} (with a Woods-Saxon density profile, an inelastic nucleon-nucleon cross section of $\sigma_{NN}^{inel} = 30$ mb, and an impact parameter range of $b = 0 - 10$ fm), we get $A_{part} = 2.5$ (3.3) for p+Nb (p+Au). Hence, we derive for our system, p+Nb, a normalized $A + \Sigma^0$ yield being about 1.9 times larger than the $K^+$ yield per number of participants for p+Au collisions at the same beam energy \cite{28}.

3.2.3 Transport model predictions

Two transport approaches are compared with the experimental data, i.e. the Ultra-relativistic Quantum Molecular Dynamics
(UrQMD) model \cite{73,74} and the Giessen Boltzmann Uehling Uhlenbeck (GiBUU) model \cite{2,88}. For UrQMD \footnote{http://urqmd.org} we used code release version 3.3p1, while for GiBUU \footnote{https://gibuu.hepforge.org} we worked with release 1.6.6179 in real-particle mode (w/o mean-field baryon-baryon potential). In GiBUU, a threshold energy of $\sqrt{s} = (3.4 \pm 0.1)$ GeV (default) steers, for baryon-baryon collisions, the smooth transition from the resonance model to the PYTHIA implementation (version 6.4.26).

Inspecting the transverse-momentum distributions within rapidity slices, $d^2N/dydp$, as displayed on a linear scale in Fig. 7, one realizes that the highest predictive power of the transport models would result from the low transverse momenta, where, however, the detector acceptance often prevents reliable experimental data. For rapidities $y \gtrsim 0.3$, both models exhibit $p_t$ spectra with shapes similar to those of the single-slope Maxwell-Boltzmann distributions fitted to the experimental data (dotted curves). In the target-rapidity range, however, the models show deviations from the one-slope shape, i.e. a superposition of differently hard spectra. The two main sources of these spectra are the contribution from first chance collisions yielding a rapidity spectrum centered around $y_{cen}$ and the contribution from subsequent hyperon-nucleon (YN) collisions slowing down the $\Lambda$'s down to target rapidity, $y = 0$. This finding could be well established by inspecting the subprocesses governing the $\Lambda$ rapidity distributions generated with the models (cf. Fig. 6). Thus, increasing in GiBUU the YN cross sections by a factor of two the $\Lambda$ yield could be partially redistributed to lower rapidities leading to a stronger enhancement around target rapidity. However, neither the shape nor the absolute yield of the experimental rapidity distribution could be reproduced.

We tested the influence of the energy threshold at which GiBUU switches from the resonance model to PYTHIA in baryon-baryon collisions. Decreasing this threshold, hence increasing the operating range of PYTHIA, the inverse slope parameter $T_B(y)$ derived from Boltzmann fits to the model distributions decreased (i.e. the spectra got softer) and the rapidity density $dN/dy$ increased, for all rapidities. E.g., for a threshold of 2.6 GeV (default value in release 1.5), $T_B(y)$ from the simulation is throughout smaller than the experimental data with a maximum of 75 MeV at $y \approx 0.7$, while the yield $dN/dy$ increases roughly by an overall factor of 1.5. Apparently, in PYTHIA some elementary cross sections being relevant for $\Lambda$ production are larger than the corresponding ones implemented into the resonance model. For a threshold of 3.3 GeV, the average $\Lambda$ yield within the detector acceptance would match the experimental one. The shape of the experimental $dN/dy$ distribution, however, could not be reproduced, i.e. the model distribution falls slower with rapidity than the experimental one (cf. Fig. 5).

Finally, on an absolute scale, the UrQMD approach does a better job than the GiBUU model, since it largely reproduces the experimental transverse-momentum and rapidity-density distributions. The ongoing analysis of inclusive $K^0$ and $\Lambda$ production in pp collisions at the same kinetic beam energy of 3.5 GeV will provide cross section measurements of quite a number of elementary reaction channels (especially $pp \rightarrow \Lambda^{+}K^{0}\Lambda/\Sigma^{0}$) and perhaps even of new channels (e.g. channels involving $\Sigma(1385)$ or $\Lambda(1405)$ \cite{89,90}) which may help to improve the resonance-model part of GiBUU.
3.3 \( \Lambda \) Polarization

\[ \mathbf{n} = \frac{\mathbf{p}_{\text{beam}} \times \mathbf{p}_\Lambda}{|\mathbf{p}_{\text{beam}} \times \mathbf{p}_\Lambda|} \]  \hspace{1cm} (2)

The relevant angle to be studied is the angle \( \zeta \) between \( \mathbf{n} \) and the momentum vector \( \mathbf{p}_\ast \) of the decay proton in the \( \Lambda \) rest frame (marked by an asterisk), i.e.

\[ \cos \zeta = \frac{\mathbf{p}_\ast \cdot \mathbf{n}}{|\mathbf{p}_\ast \cdot \mathbf{n}|}. \]  \hspace{1cm} (3)

\[ \frac{dN}{d\cos \zeta} = C'(1 + \alpha \mathcal{P} \cos \zeta) \]  \hspace{1cm} (4)

to the distribution of the corrected (experimental/simulation) angular distribution shown in the lower panel of Fig. 8. Note that in Eq. (4), the asymmetry parameter, \( \alpha = 0.642 \pm 0.013 \), of the parity-violating weak decay of the \( \Lambda \) hyperon is a measure of the interference between s and p waves of the final state [71].

The corresponding experimental angular distribution is displayed in the upper panel of Fig. 8. It is derived similarly to the filling of the raw phase-space distribution of the \( \Lambda \), i.e. performing, for each angular bin \( d\cos \zeta \), a combinatorial-background subtraction on the proton-\( \pi^- \) invariant-mass distribution with subsequent \( \Lambda \)-peak integration. The corresponding (polarization-free) UrQMD-simulated angular distribution is given in the middle panel of Fig. 8. The yield suppression around \( \cos \zeta \sim 0 \) is the result of the detector acceptance. Both, the experimental and simulated, angular distributions exhibit a high degree of mirror symmetry w.r.t. the \( \Lambda \) production plane. Since the \( \Lambda \) statistics is copious, we extract the \( \Lambda \) polarization \( \mathcal{P} \) by fitting a straight line

\[ \frac{dN}{d\cos \zeta} = C'(1 + \alpha \mathcal{P} \cos \zeta) \]  \hspace{1cm} (4)

\[ \mathcal{P} = \frac{2 \mathcal{U}_\text{up} - \mathcal{U}_\text{down}}{\alpha} \]  \hspace{1cm} (5)

(Another, equivalent, approach to the polarization is based on the relation \( \alpha \mathcal{P} = \langle \cos \zeta \rangle / \langle \cos^2 \zeta \rangle \), where the angle brackets

\[ \mathcal{P} = \frac{2 \mathcal{U}_\text{up} - \mathcal{U}_\text{down}}{\alpha} \]  \hspace{1cm} (5)

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imply the average over the entire angular range and all events.) The corresponding overall polarization derived with Eq. (5) amounts to $-0.104 \pm 0.008 \pm 0.027$, in agreement with the values derived with the linear fit. The mean value following from the various methods amounts to $(\mathcal{P}) = -0.119 \pm 0.005 \pm 0.016$ with the given statistical and systematic errors. For the differential $\Lambda$ polarization investigated in the following, the linear fit with Eq. (4) is used, and the systematic errors are accounted for by method (1).

Now, we study the phase-space dependence of the $\Lambda$ polarization. Figure 9 shows the $\Lambda$ polarization as a function of rapidity and transverse momentum, $\mathcal{P}(y, p_t)$. Note that, for this (quasi triple-differential) figure, sixteen hundred invariant-mass distributions of proton-$\pi^-$ pairs have been analyzed (i.e., 8 topological cut sets, 8 $\cos \zeta$ bins, 5 $p_t$ bins, 5 $y$ bins). We exclusively observe negative central polarizations values over the entire phase space displayed. Even when incorporating the given errors, this finding keeps almost unchanged. Though the statistics is copious, the absolute value of the polarization is somewhat fluctuating, i.e. it shows differences between the central values determined in neighbouring phase-space cells. Typically, these deviations of the polarization values from the average trends in slices of rapidity or transverse momentum (determined, e.g., by linear regression), are well within the errors. A clear tendency from the lower right to the upper left corner is found: The polarization is strongest at low rapidities and large transverse momenta. Its absolute value increases with transverse momentum for the two lowest rapidity bins while it is almost independent of $p_t$ within the remaining $y$ region; and it decreases with rapidity for the three upper transverse-momentum bins while it hardly changes with rapidity for the two low-$p_t$ bins.

To make this finding more obvious, we studied the one-dimensional dependences. For that reason, we included also the regions outside the sharp upper and lower rapidity and transverse-momentum limits of Fig. 9 which were applied for statistical reasons. Integrating over all experimentally populated rapidities, Fig. 10 shows the dependence of the $\Lambda$ polarization on the $\Lambda$ transverse momentum. Its absolute value clearly increases with $p_t$. The dotted line is a linear fit to the data with the simplest formula ensuring a vanishing polarization at zero transverse momentum, i.e. $\mathcal{P}(p_t) = D p_t$. The corresponding slope amounts to $D = (-0.18 \pm 0.02) (\text{GeV/c})^{-1}$. Looking for phase-space dependences of earlier measurements one realizes that, because of the fixed $\Lambda$ production angle in most of the high-energy experiments, a definite Feynman-$x$ value corresponds to a certain transverse momentum. Hence, there the $p_t$ dependence of the $\Lambda$ polarization reflects both $p_t$ and $x_F$-dependences. Nevertheless, our slope $D$ is well in between the $p_t$ slopes of about -0.05 to -0.30 (GeV/c)$^{-1}$ found for pN-reactions at energies from 400 to 800 GeV and presented in the compilation of ref. [56].

Integrating instead over all experimentally accessible transverse momenta, Fig. 11 gives the rapidity dependence of the $\Lambda$ polarization, $\mathcal{P}(y)$. Its absolute value is smallest at an intermediate rapidity, $y \simeq 0.82 \pm 0.09$, as derived from a parabolic fit (dotted curve) to the experimental data, and increases weakly both with decreasing and increasing rapidity, whereby the behaviour at the upper rapidities is compatible with a constant polarization. It is worth to recall that $\Lambda$ polarization in pp collisions is odd in $x_F$ (or $(y-y_{cm})$) with negative (positive) sign in the beam (target) fragmentation region [38,43,47]. In the present experiment, however, the $\Lambda$ hyperons carry exclusively negative polarizations while they populate mostly the target hemisphere (Fig. 6). Hence, the number of $\Lambda$‘s arising from primary (first chance) pN collisions is negligible, and the polarization we see at low rapidities is supposed to come from $\Lambda$‘s which have scattered, which are produced by slowed-down beam protons, or which are produced by “unwounded” protons on a cluster of many nucleons from the target.

4 Summary

Summarizing, we presented high-statistics data on production and polarization of $\Lambda$ hyperons produced in collisions of p(3.5 GeV)+Nb. The data were taken with HADES at SIS18/GSI. The $\Lambda$ phase-space distribution was compared with corresponding results of other experiments and with transport model predictions. The rapidity density was found to decrease monotonically within a rapidity window ranging from 0.3 to 1.3, i.e. from values above the target rapidity to values beyond the center-of-mass rapidity for nucleon-nucleon collisions. None of the employed models was able to reproduce fully the experimental distributions, i.e. in absolute yield and in shape. We link this observation to an insufficient modelling in the transport approaches of the elementary processes being relevant for $\Lambda$ production, rescattering and absorption. For the first time, the data allow for a genuine two-dimensional
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Fig. 10. \( \Lambda \) polarization as a function of the \( \Lambda \) transverse momentum, \( \mathcal{P}(p_t) \). The vertical bars associated with symbols represent the combined statistical and systematic errors. The dotted curve is a fit to the data with a straight line (cf. text).

Fig. 11. \( \Lambda \) polarization as a function of the \( \Lambda \) rapidity, \( \mathcal{P}(y) \). The vertical bars associated with symbols represent the combined statistical and systematic errors. The dotted curve is a fit to the data with a parabola (cf. text). The arrow indicates the center-of-mass rapidity in nucleon-nucleon collisions at 3.5 GeV.

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