The effect of including molecular opacities of variable composition on the evolution of intermediate-mass AGB stars

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ABSTRACT
Calculations from stellar evolutionary models of low- and intermediate-mass asymptotic giant branch (AGB) stars provide predictions of elemental abundances and yields for comparison to observations. However, there are many uncertainties that reduce the accuracy of these predictions. One such uncertainty involves the treatment of low-temperature molecular opacities that account for the surface abundance variations of C, N and O. A number of prior calculations of intermediate-mass AGB stellar models that incorporate both efficient third dredge-up and hot bottom burning include a molecular opacity treatment which does not consider the depletion of C and O due to hot bottom burning. Here we update the molecular opacity treatment and investigate the effect of this improvement on calculations of intermediate-mass AGB stellar models. We perform tests on two masses, 5 and 6 M☉, and two metallicities, Z = 0.001 and 0.02, to quantify the variations between two opacity treatments. We find that several evolutionary properties (e.g. radius, T eff and T bce) are dependent on the opacity treatment. Larger structural differences occur for the Z = 0.001 models compared to the Z = 0.02 models indicating that the opacity treatment has a more significant effect at lower metallicity. As a consequence of the structural changes, the predictions of isotopic yields are slightly affected with most isotopes experiencing changes up to 60 per cent for the Z = 0.001 models and 20 per cent for the Z = 0.02 models. Despite this moderate effect, we conclude that it is more fitting to use variable molecular opacities for models undergoing hot bottom burning.

Key words: nuclear reactions, nucleosynthesis, abundances – stars: AGB and post-AGB – stars: Population II – ISM: abundances.

1 INTRODUCTION
The asymptotic giant branch (AGB) phase is the last nuclear burning stage for low- and intermediate-mass stars with initial masses of between ~0.8 and ~8 M☉ (see Herwig 2005 for a review). During their evolution on the AGB, stars in this mass range experiencing episodes that dredge up newly synthesized material which contains the products of He burning and neutron-capture nucleosynthesis into the convective envelope (see Busso, Gallino & Wasserburg 1999 for a review). Combined with strong mass loss that ejects the stellar envelope into the interstellar medium, low- and intermediate-mass AGB stars are important contributors to the chemical evolution of the Galaxy (for example, Romano et al. 2010; Kobayashi, Karakas & Umeda 2011; Recio-Blanco et al. 2012). This study is concerned with the evolution of intermediate-mass stars on the AGB with an initial mass ≥4 M☉. These stars produce substantial primary nitrogen and are predicted to produce nitrogen-enhanced metal-poor stars in the early Galaxy (e.g. Pols et al. 2012). Intermediate-mass AGB stars are also implicated in the chemical evolution of globular clusters (Gratton, Sneden & Carretta 2004; Ventura, Carini & D’Antona 2011). However, the modelling of the evolution and nucleosynthesis of low- and intermediate-mass AGB stars is dependent on highly uncertain input physics including convection, mass loss, reaction rates and opacity.

Briefly, the structure of an AGB star consists of an electron-degenerate CO core surrounded by a He-burning shell and a H-burning shell which are separated by the He intershell. This is encompassed by a deep convective envelope. During the thermally pulsing AGB (TP-AGB) phase, the star undergoes periodic thermal pulses (TPs) due to instabilities in the He-burning shell (Busso et al. 1999; Herwig 2005). During the evolution of a TP-AGB star, two known mechanisms can occur which can periodically alter the surface composition: third dredge-up (TDU) and hot bottom burning (HBB). When the He-burning shell becomes unstable, it drives an expansion of the star in order to release the energy generated by He burning. A flash-driven convective zone forms in the He-intershell mixing material, mainly 12C, from the base of the He
shell throughout the intershell region. The outer layers have been cooled by the expansion and the H-burning shell has been almost extinguished which allows the outer convective envelope to move inwards. If the convective envelope reaches into the He intershell, $^{12}{\text{C}}$ and the products of slow neutron-capture nucleosynthesis (the s-process) are mixed to the surface. This process of TDU can occur multiple times and is responsible for creating carbon-rich stars with a C/O ratio greater than unity.

HBB occurs in stars with masses greater than approximately $4\,M_\odot$ depending on metallicity and the input physics used. HBB takes place during the interpulse phase between TPs when the base of the outer convective envelope penetrates into the H-burning shell and becomes hot enough to sustain proton-capture nucleosynthesis. The CNO cycle converts $^{12}{\text{C}}$ and $^{16}{\text{O}}$ that has been mixed into the envelope by TDU into predominately $^{14}{\text{N}}$. Therefore, HBB can prevent the stellar surface from becoming carbon rich by decreasing the $^{12}{\text{C}}$ abundance in the envelope. Frost et al. (1998) presented evolutionary calculations of intermediate-mass AGB stellar models and found that the surface C/O ratio initially decreases due to HBB. However, mass loss slowly erodes the envelope causing a decrease in envelope mass. This results in a lower temperature at the base of the convective envelope which causes HBB to cease. There is also less dilution of the dredged-up material. This means that the C/O ratio starts to increase at the end of the TP-AGB phase, and in some cases, to reach above unity.

Mass loss and convection have been shown to dominate modelling uncertainties in intermediate-mass AGB models (Ventura & D’Antona 2005a,b; Stancliffe & Jeffery 2007; Karakas, García-Hernández & Lagar 2012). However, other uncertainties including reaction rates and opacities have been shown to affect the stellar structure and therefore the yields (Izzard et al. 2007; Ventura & Marigo 2009). In recent years there has been considerable work developing accurate low-temperature molecular opacities for stellar evolution calculations (Marigo & Aringer 2009). Due to these improvements to the opacity input physics, it is now possible to quantify the effect of the updated opacities on the stellar evolution calculations and yield predictions (Ventura & Marigo 2009; Weiss & Ferguson 2009).

Intermediate-mass AGB stars have been shown to have effective temperatures low enough for dust and molecule formation at solar metallicity and in the Magellanic Clouds (García-Hernández et al. 2009). In particular, we also show in this study that low-metallicity AGB stars become cool enough to form molecules particularly once they become carbon rich. The opacity tables of Alexander & Ferguson (1994), and later Ferguson et al. (2005), include a detailed treatment of the inclusion of molecules to the total opacity at low temperatures where $T \lesssim 10^4$ K. These tables, however, are only available for solar or scaled-solar composition. As previously mentioned, low- and intermediate-mass AGB stars undergo mixing episodes that alter their surface composition in a complex way. In particular, low-mass AGB stars can become carbon rich and intermediate-mass stars can display a range of behaviours for the C/O ratio. Marigo (2002) shows that, at the transition point when the C/O ratio goes from below unity to above unity, the dominant source of molecular opacity changes from oxygen-bearing molecules to carbon-bearing molecules. In AGB models, this causes a sudden decrease of the effective temperature and an expansion in radius which in turn increases the rate of mass loss. It is therefore necessary to use low-temperature molecular opacities that follow the change in the C/O ratio with time. The low-temperature opacity tables of Lederer & Aringer (2009) only account for an enhancement in C and N compared to initial abundances whereas the ÁESOPUS opacity tables of Marigo & Aringer (2009) are able to account for the depletion and enhancement of C, N and the C/O ratio.

Using the ÁESOPUS molecular opacity tables, the effects of molecular opacities on the evolution of AGB stellar models have been investigated by Ventura & Marigo (2009, 2010). Using two different opacity treatments, they determine that the yields of C, N, O and Na can be significantly altered depending on the opacity prescription used. Ventura & Marigo (2010) stress that it is important to use a molecular opacity treatment that accounts for variations in the surface CNO abundance when the C/O ratio exceeds unity. They find a minimum threshold mass for AGB stellar models ($\geq 3.5\,M_\odot$ for $Z = 0.001$) where the use of opacity tables that account for the variations in the surface CNO abundance becomes less important. This is because HBB prevents the C/O ratio from exceeding unity for all their models with a mass greater than $3.5\,M_\odot$ rather than the models not being cool enough to form molecules. The models of Ventura & Marigo (2010) have very efficient HBB owing to their choice of convective model, the full spectrum of turbulence (FST) prescription (Canuto & Mazzitelli 1991) and little TDU due to how they treat the convective borders.

As intermediate-mass AGB stars can experience both TDU and HBB, the complex interplay between the two processes can cause the star to become either oxygen rich or carbon rich. Stellar models calculated with different stellar evolution codes can display varied behaviours including differences in the efficiency of TDU and HBB which can alter the surface C/O ratio allowing for either carbon- or oxygen-rich compositions. This in turn means that the effect of the molecular opacities on the stellar evolution can vary greatly depending on model assumptions. In contrast, low-mass AGB stars only experience TDU which serves to increase the surface C/O ratio.

The aim of this paper is to expand upon the work of Ventura & Marigo using intermediate-mass AGB models that show a different evolution of the surface C/O ratio. In particular, our low-metallicity models show very deep dredge-up and become carbon rich during the AGB phase in contrast to the models of, for example, Ventura & Marigo (2010). Therefore, their conclusions are not necessarily applicable to our models. The paper is presented as follows. In Section 2, we describe the method of calculation we use to model an AGB star and detail the molecular opacities used in the investigation. In Section 3, we present the results of the stellar models and in Section 4 we present the effect on the yields for the two opacity treatments. In Section 5, we compare with previous studies and summarize our results.

2 NUMERICAL METHOD

A two-step procedure is used to calculate each AGB stellar model. First, we use the Mt Stromlo stellar evolutionary code (Karakas, Campbell & Stancliffe 2010, and references therein) to calculate the stellar evolutionary sequences. Each stellar model was evolved from the zero-age main sequence to near the end of the TP-AGB phase when the majority of the convective envelope is lost by strong stellar winds. For convective regions, we use the standard mixing length theory (MLT; Böhm-Vitense 1958) with a mixing length parameter of $\alpha = 1.86$. The details of the procedure and the evolution code are described in Karakas et al. (2010) with the following differences. We update the low-temperature molecular opacities (described in detail in Section 2.2) and the high-temperature radiative opacity tables. To be consistent with the molecular opacity tables, we use OPAL radiative tables (Iglesias & Rogers 1996) with a Lodders (2003) scaled-solar abundance. We do not include convective overshoot in the formal sense in order to obtain the TDU. However, we follow
the method described by Lattanzio (1986) and Frost & Lattanzio (1996) to determine a neutral border to each convective boundary. In this method, the ratio of the temperature gradients is linearly extrapolated from the last two convective mesh points to the first radiative point. If the extrapolated value is greater than unity, then the point is determined to be in the convective zone, and if less than unity the point is considered to be in the radiative zone. This means that only one point can be added, per iteration, to the convective zone.

The calculated stellar evolutionary sequences are used as input into a post-processing nucleosynthesis code (see Cannon 1993; Lugaro et al. 2004). The nuclear network we use is based on the JINA Reaclib1 data base as of 2012 May (Cyburt et al. 2010). It includes 589 reactions of 77 species from hydrogen to sulphur with a small group of iron-peak elements (Fe, Co and Ni). An additional ‘species’ $g$ is included in the network to account for the number of neutron captures occurring beyond $^{60}$Ni; this $g$ species simulates the $s$-process as a neutron sink. We use a scaled-solar initial composition from Asplund et al. (2009) and assume a global metallicity of $Z = 0.015$ which is comparable to the solar global metallicity recommended by Asplund et al. (2009) of $Z = 0.0142$. This differs from the Lodders (2003) solar metallicity of 0.013 21 in the opacity tables as low-temperature opacity tables using the Asplund et al. (2009) values are not available. Throughout this paper, all abundance ratios are by number whereas individual species are in mass fraction. We assume that the envelope abundances are equivalent to surface abundances.

2.1 Mass loss

We assume the same mass-loss formula for all our models. Mass loss prior to the AGB phase is included using the Reimers (1975) formula with $\eta_R = 0.4$. This leads to very little mass being lost before the AGB phase. For example, the intermediate-mass models presented here lose less than 1 per cent of their initial mass before they reach the early AGB phase.

Mass loss is included during the AGB phase using the Vassiliadis & Wood (1993) mass-loss prescription where only their equation 2 is used. The empirical formula of Vassiliadis & Wood (1993) was determined using a sample of oxygen- and carbon-rich AGB stars in the Milky Way and Magellanic Clouds which cover a range of luminosities and pulsation periods.

2.2 Molecular opacities

Bound–bound absorption by molecules becomes an important contribution to the total opacity at temperatures below 5000 K (Alexander & Ferguson 1994). The abundance of carbon relative to oxygen in the stellar envelope can significantly influence the formation of molecules and has a substantial effect on the opacity at low temperatures. Changes in the stellar envelope opacity occur when the stellar envelope transitions from an oxygen-rich (C/O < 1) to a carbon-rich (C/O > 1) chemical composition (Marigo & Aringer 2009). This is due to the excess of carbon atoms allowing for the formation of carbon-bearing molecules such as, for example, HCN, CN, C$_2$ and SiC.

The intermediate-mass stellar models of Karakas et al. (2012) use low-temperature molecular opacity tables from Lederer & Aringer (2009) that account for only an increase in C due to TDU. For low-mass AGB stellar models that do not undergo HBB, this method is sufficient as TDU will only increase the C abundance in the envelope. However, for intermediate-mass stars, CNO cycling during HBB causes a decrease in the C abundance (as well as the O abundance) in the envelope and it is possible that the C abundance will become lower than the initial C abundance. The subsequent decrease in O along with C can still cause the star to have a C/O ratio above unity. The opacity tables used in Karakas et al. (2012) do not account for this. In order to account for these variations, we include low-temperature opacity tables to follow the decrease in C and O due to HBB.

For the stellar models presented here, we use the ÆSOPUS low-temperature molecular opacity tables (Marigo & Aringer 2009) with a Lodders (2003) scaled-solar abundance. The low-temperature opacity tables have been calculated to follow the variations in the chemical composition of C, N and O in the envelope due to TDU and HBB. The tables use Rosseland mean opacities and are a function of temperature $\log(T)$ and $\log(R)$ where $R = \rho/(T/10^{10})K^{-1}$ for an arbitrary chemical composition (Marigo & Aringer 2009). We use linear interpolation between tables with $\log(T)$ from 3.2 to 4.05 in steps of 0.05 dex and $\log(R)$ from $-7.0$ to $1.0$ in steps of 0.5 dex.

To account for the changes in C, N and O in the envelope due to TDU and HBB, a variation factor $f_i$ is used,

$$X_i = f_i X_{i,ref},$$

where $X_i$ is the current abundance of species $i$ in mass fraction and $X_{i,ref}$ is the initial reference abundance of species $i$. A value of $f_i > 1$ indicates an enhancement in the abundance whereas $f_i < 1$ indicates a depletion in the abundance compared to the initial reference abundance. The increase (or decrease) in abundance for C, N and O can be described using the following equations from Ventura & Marigo (2009):

$$\frac{X_C}{X_O} = f_C \frac{X_{C,ref}}{X_{O,ref}},$$

$$X_C = f_C X_{C,ref},$$

$$X_N = f_N X_{N,ref}.$$ 

The helium abundance is then given by $Y = 1 - X - Z$ so that the composition conserves mass where $X$ is the hydrogen abundance and $Z$ is the global metallicity.

We perform tests using two opacity treatments: one which only accounts for the increase in C (referred to as $\kappa_C$) and another where the increase and decrease in C and O are accounted for (referred to as $\kappa_{CO}$). The $f_i$ values used in this study for C, N and CO are detailed in Table 1. We use the same scaled-solar ÆSOPUS opacity tables as used by Kamath, Karakas & Wood (2012) for the $\kappa_C$ models. In the $\kappa_{CO}$ models, we incorporate two additional variation factors for C and the C/O ratio and explicitly follow the envelope C/O ratio to account for a possible reduction in C and O abundances due to HBB for the $\kappa_{CO}$ models. The variations in abundance of N are treated the same for all models.

3 STELLAR MODELS

3.1 Stellar structure

We model two stellar masses, namely 5 and 6 $M_\odot$, with two metallicities, $Z = 0.001$ and 0.02, to determine the effect of the two

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1 https://groups.nscl.msu.edu/jina/reaclib/db/
Table 1. Values of $f_i$ factors for the calculation of molecular opacity for the $\kappa_C$ and $\kappa_{CO}$ stellar models. The additional values included in the $\kappa_{CO}$ treatment are shown in bold.

| $Z$  | $X$  | $\log(f_C/\alpha)$ | $\log(f_C)$ | $\log(f_i)$ | C/O |
|------|------|-----------------|-------------|-------------|-----|
| 0.001| 0.5  | $-1.00$         | $-1.00$     | 0.00        | 0.050 |
| 0.6  | $-0.35$ | $-0.35$       | 0.60        | 0.224       |
| 0.7  | 0.00  | 0.00            | 1.20        | 0.501       |
| 0.8  | 0.17  | 0.17            | 0.741       |
| 0.30  | 0.30  | 1.000           |
| 0.35  | 0.35  | 1.122           |
| 0.90  | 0.90  | 3.980           |
| 1.55  | 1.55  | 17.779          |
| 2.17  | 2.17  | 74.114          |
| 0.02  | 0.5  | $-1.00$         | $-1.00$     | 0.00        | 0.050 |
| 0.6  | $-0.35$ | $-0.35$       | 0.60        | 0.224       |
| 0.7  | 0.00  | 0.00            | 0.30        | 0.501       |
| 0.8  | 0.17  | 0.17            | 0.741       |
| 0.25  | 0.25  | 0.891           |
| 0.30  | 0.30  | 1.000           |
| 0.35  | 0.35  | 1.122           |
| 0.50  | 0.50  | 1.585           |
| 0.70  | 0.70  | 2.511           |

Table 2. Properties of the calculated stellar models. Column 1 lists the opacity treatment, column 2 the initial mass, column 3 the initial global metallicity, column 4 the number of TPs calculated, column 5 the final core mass, column 6 the final envelope mass, column 7 the maximum temperature reached at the base of the convective envelope and column 8 the total amount of material dredged up due to TDU.

$$
\begin{array}{cccccccc}
\text{Opacity} & \text{Mass} & Z & \text{TPs} & \text{Final } M_{\text{core}} & \text{Final } M_{\text{env}} & T_{\text{max}} & M_{\text{dred}} \\
\text{(M}_\odot\text{)} & \text{(M}_\odot\text{)} & \text{Z} & & \text{(M}_\odot\text{)} & \text{(M}_\odot\text{)} & (\times 10^6 \text{ K}) & \text{(M}_\odot\text{)} \\
\kappa_C & 5.0 & 0.001 & 108 & 0.940 & 0.960 & 92.99 & 0.216 \\
& 6.0 & 0.001 & 126 & 1.018 & 0.888 & 104.91 & 0.127 \\
& 5.0 & 0.02 & 30 & 0.868 & 0.713 & 63.29 & 0.088 \\
& 6.0 & 0.02 & 41 & 0.907 & 1.084 & 81.59 & 0.090 \\
\kappa_{CO} & 5.0 & 0.001 & 96 & 0.938 & 1.035 & 92.47 & 0.192 \\
& 6.0 & 0.001 & 112 & 1.015 & 0.662 & 104.79 & 0.107 \\
& 5.0 & 0.02 & 29 & 0.867 & 1.013 & 63.95 & 0.083 \\
& 6.0 & 0.02 & 42 & 0.908 & 1.352 & 82.30 & 0.092 \\
\end{array}
$$

It can be seen that the updated opacity treatment $\kappa_{CO}$ model has 12 fewer TPs while the $6 \text{ M}_\odot$, $Z = 0.001 \kappa_C$ model has 12 fewer TPs when compared to the $\kappa_C$ models. This means that less enriched material is dredged up to the surface as demonstrated in Table 2 where the total amount of He-intershell material decreases by around 15 per cent for the $\kappa_{CO}$ models. The $Z = 0.001 \kappa_C$ models each dredge up approximately 0.02 $\text{M}_\odot$ more material over the lifetime of the AGB phase compared to the $\kappa_{CO}$ models.

The evolution of the temperature at the base of the convective envelope for each model is shown in Fig. 2 (panels a and b). HBB is evident as the temperature reaches higher than the (50–80) $\times 10^6$ K required for CNO cycling at the base of the convective envelope. Fig. 2 for the $Z = 0.001$ models shows that, when using the updated opacity tables $\kappa_{CO}$, HBB is extinguished earlier. This is because the $\kappa_{CO}$ models become more extended in radius and therefore cooler. This change due to the increased molecular opacity leads to an enhanced mass-loss rate which ejects the envelope sooner.

Fig. 3 (panels a and b) compares the evolution of the C/O ratio between the two opacity treatments for both $Z = 0.001$ models. For a period during the AGB phase, the competing effects of TDU and HBB can cause the C/O ratio to fluctuate between below unity and above unity. For a brief time during this period, the $^{12}$C surface abundance is below the initial $^{12}$C surface abundance while the C/O ratio is greater than unity. The molecular opacity is then underestimated in the $\kappa_C$ model as the fact that the C/O ratio exceeds unity has not been taken into account during these conditions. This omission in the determination of the opacity results in the discrepancies seen in the stellar evolution between the $\kappa_C$ and $\kappa_{CO}$ models in Fig. 4. Fig. 4 shows the temporal evolution of the C/O ratio, $^{12}$C surface abundance, $^{16}$O surface abundance, effective temperature and mass-loss rate for the $5 \text{ M}_\odot$, $Z = 0.001$ models.

As mentioned by Marigo (2002), the consequences of using opacity tables that do not correctly follow the variation of the C/O ratio when the star is carbon rich include an inaccurate effective temperature. Fig. 4 shows that the difference between the $\kappa_C$ and $\kappa_{CO}$ models, around 0.001 $\text{M}_\odot$ for the $5 \text{ M}_\odot$ model. This can be attributed to minor differences during core He-burning evolution. It can be seen that the updated opacity treatment $\kappa_{CO}$ reduces the number of TPs during the AGB phase for the $Z = 0.001$ models.
models is not due to a slightly different core mass at the beginning of the TP-AGB phase. The lower effective temperature (panel d) and higher mass-loss rate (panel e) for the $\kappa_{\text{CO}}$ models start to become significant when the surface C/O ratio for the models changes from below unity to above unity. This is where the $\kappa_{\text{CO}}$ molecular opacity treatment more realistically follows the increase in the C/O ratio.

### 3.1.2 $Z = 0.02$ models

The effect of the different opacity treatment on the number of TPs is less pronounced for the $Z = 0.02$ models than for the $Z = 0.001$ models. Fig. 1 (panel b) shows that the difference in the evolution of the mass of the H-exhausted core between the two opacity treatments is very slight for the $6 M_\odot$ model. The differences between the two opacity treatments are minimal, and the C/O ratio of the models does not exceed unity which would result in a higher molecular opacity where carbon-bearing molecules dominate. Compared to the $Z = 0.001$ models, there are fewer TPs with a shorter lifetime of the TP-AGB phase. The $5 M_\odot$ $\kappa_{\text{CO}}$ model experiences one less TP while the $6 M_\odot$ $\kappa_{\text{CO}}$ model experiences one more TP than the $\kappa_C$ models. We conclude that the differences in the number of TPs are insignificant.

Fig. 5 shows the evolution of the C/O ratio, $^{12}$C surface abundance, $^{16}$O surface abundance, effective temperature and mass-loss rate for the TP-AGB phase for the $6 M_\odot$ model. Pre-AGB evolution mixing episodes cause the surface $^{12}$C and $^{16}$O abundances to
The variation of the C and O abundances as only the increase in the $^{12}$C abundance is taken into account.

For the $\kappa_C$ 6 $M_\odot$ model, this situation where the current C/O, C and O abundances are never greater than the initial abundances is treated as if the surface abundance has a scaled-solar composition. The low-temperature molecular opacity does not vary for a given temperature and density with the variation factors being $f_C = f_O = 0$. Fig. 6 shows the opacity below $\log(T) \lesssim 4$ in the 6 $M_\odot$ $\kappa_C$ and $\kappa_{CO}$ models for the same total stellar mass of approximately 2.3 $M_\odot$. This snapshot was chosen where the opacity difference is largest. At $\log(T) \lesssim 3.5$ near the stellar surface, the opacity is lower for the $\kappa_{CO}$ model compared to the $\kappa_C$ model. This decrease in opacity leads to a decrease below initial values. This causes the C/O ratio to decrease with the C/O ratio being below the initial value at the start of the TP-AGB phase. HBB is only active for part of the TP-AGB evolution in the 6 $M_\odot$, $Z = 0.02$ models. This is illustrated in Fig. 5 (panel a) where the C/O ratio initially increases, albeit with a shallow gradient and then decreases once the temperature at the base of the envelope becomes high enough for proton captures on to $^{12}$C. Eventually, HBB is extinguished and the C/O ratio increases to almost its initial value owing to the continuation of TDU. It is when HBB is active that the $\kappa_C$ model does not accurately follow the variation of the C and O abundances.
higher effective temperature (as seen in the bottom panel of Fig. 5), and as a consequence the mass-loss rate is lower and HBB ceases slightly later. The sustained level of HBB causes a lower final C/O ratio compared to the $\kappa_C$ models as seen in Fig. 5 (panel a).

### 3.2 Stellar yields

In order to determine the total amount of material ejected into the interstellar medium during the lifetime of the stellar model, we calculate the net yield $M_i$ (in solar masses) of species $i$ to be

$$M_i = \int_0^\tau [X(i) - X_0(i)] \frac{dM}{dt} \, dt,$$

where $dM/dt$ is the current mass-loss rate in $M_\odot$ yr$^{-1}$, $X(i)$ and $X_0(i)$ are the current and initial mass fraction of species $i$, and $\tau$ is the total lifetime of the stellar model in years. After calculating the stellar yields, we calculate the percentage change $\Delta M_i$ for each stable isotope where $M_{i,C}$ is the yield for species $i$ using the $\kappa_C$ models and $M_{i,\kappa CO}$ is the yield for species $i$ using the $\kappa_{CO}$ models. The percentage change in yields between the $\kappa_C$ and $\kappa_{CO}$ models for each mass and metallicity is shown in Fig. 7. The changes in surface abundance, and consequently the final net yield, are dependent on the amount of material dredged up from the He intershell as well as the maximum temperature and duration of HBB. Yields for selected isotopes are presented in Table 3 for the two opacity treatments, $\kappa_C$ and $\kappa_{CO}$.

#### 3.2.1 Z = 0.001 yields

Fig. 7 (panels a and b) shows that the 5 and 6 $M_\odot$, $Z = 0.001$ models display a similar trend in yield differences between the two opacity treatments, $\kappa_C$ and $\kappa_{CO}$. Percentage changes of up to 30 per cent are seen for the 5 $M_\odot$ model whereas the 6 $M_\odot$ model shows percentage changes of up to 60 per cent in the yield. However, the yield of $^{19}$F decreases by 250 per cent for the 5 $M_\odot$ models which is not seen in the 6 $M_\odot$ models. The reduced number of TDU episodes for the $\kappa_{CO}$ models influences the changes seen in the yields. A higher percentage change is seen in the yields for the 6 $M_\odot$ model compared to the 5 $M_\odot$ model. This is caused by a larger decrease in the number of TPs as well as the shorter duration of HBB between the $\kappa_C$ and $\kappa_{CO}$ models.

### 3.2.2 Z = 0.02 yields

Fig. 7 (panels c and d) shows yield differences of up to 20 per cent for lighter isotopes with an atomic mass up to about 18 including the CNO isotopes for the $Z = 0.02$ models. For $^{19}$F we find a difference of around 15 per cent for the 6 $M_\odot$ model with a smaller difference for the 5 $M_\odot$ model. For the intermediate-mass isotopes, which include here $^{22}$Ne, $^{23}$Na, $^{25}$Mg, $^{26}$Mg and $^{28}$Al, we find very small yield differences of less than 10 per cent for both the 5 and 6 $M_\odot$ models as illustrated in Fig. 7. There is a negligible effect on the net yield of the neutron sink $g$ with a percentage change of less than 5 per cent.

From Fig. 7, we can see that the relative size of the yield changes between the $\kappa_C$ and $\kappa_{CO}$ models is smaller than that for the $Z = 0.001$ models. This is mainly because the $\kappa_C$ and $\kappa_{CO}$, $Z = 0.02$ models experience almost the same number of TPs (as shown in Table 2). In Table 3, we see that the $^{12}$C yields of the 5 $M_\odot$ models are positive compared to the negative $^{12}$C yields of the 6 $M_\odot$ models.
This indicates that there is an overall net production of carbon in the 5 M⊙ models. While the amount of material dredged into the envelope is similar in both the 5 and 6 M⊙ models (e.g. see Table 2), the maximum temperature at the base of the envelope in the 5 M⊙ is considerably lower. This means that HBB is not very efficient in the 5 M⊙ as shown in Fig. 2, where the maximum temperature is only 64 × 10⁶ K compared to 82 × 10⁶ K for the 6 M⊙ models and this temperature is only sustained for about five TPs. This means that the carbon dredged to the surface is not as efficiently burnt via the CNO cycles at the base of the envelope.

However, both κCO models have a decrease in the 12C yields compared to the κC models. In particular, the 5 M⊙ κCO model has a decrease of 80 per cent compared to the κC model. This decrease in 12C can be attributed to the longer duration, as well as the higher temperatures, of HBB. This is despite the slight differences in the number of TDU episodes. The negative yield of 16O indicates that more is being destroyed through HBB than being mixed from the intershell region to the surface. The longer duration of HBB also explains the increase in the 14N yield as more 12C is burnt to produce 14N via the CNO cycles.

**Figure 7.** The percentage change in yield for species i between the κC and κCO models for each model calculated where $\Delta M_i = 100(M_{i,\text{CO}} - M_{i,\text{C}})/|M_{i,\text{C}}|$. For the 5 M⊙ Z = 0.001 model, the percentage change for 16F is not shown. For the κCO model, the 16F yield decreases by around 250 per cent. For the 5 M⊙, Z = 0.02 models, the percentage change in 7Li and 13C is not shown. For the κCO model, the yield of 7Li decreases by around 100 per cent while the yield of 13C decreases by around 80 per cent compared to the κC model. Each plot has the same y-axis scale for each metallicity for ease of comparison.

**Table 3.** Net yields of selected isotopes. Yields are in solar masses and are expressed in the form $n(m) = n \times 10^m$.

| Opacities | Mass  | Z    | 12C     | 13C     | 14N     | 16O     | 22Ne   | 23Na   | 25Mg   | 26Mg   | g     |
|-----------|-------|------|---------|---------|---------|---------|--------|--------|--------|--------|-------|
| κC        | 5.0   | 0.001| 1.652   | 5.718   | 5.715   | -8.273  | 1.845  | 4.725  | 3.399  | 2.866  | 1.793 |
|           | 6.0   | 0.001| 9.784   | 4.298   | 3.806   | -1.547  | 5.404  | 6.487  | 2.197  | 1.279  | 1.241 |
|           | 5.0   | 0.02 | 1.864   | 3.476   | 1.971   | -2.831  | 1.720  | 9.558  | 1.563  | 8.990  | 8.321 |
|           | 6.0   | 0.02 | -1.112  | 5.849   | 4.305   | -7.224  | 1.637  | 1.350  | 2.039  | 1.248  | 1.268 |
| κCO       | 5.0   | 0.001| 2.101   | 5.447   | 5.030   | -8.422  | 1.495  | 3.763  | 2.991  | 2.292  | 1.473 |
|           | 6.0   | 0.001| 1.309   | 3.877   | 3.091   | -1.621  | 4.166  | 2.717  | 1.989  | 8.397  | 8.665 |
|           | 5.0   | 0.02 | 3.780   | 3.238   | 2.156   | -2.862  | 1.691  | 9.566  | 1.512  | 8.759  | 8.183 |
|           | 6.0   | 0.02 | -1.207  | 5.589   | 4.509   | -7.817  | 1.665  | 1.332  | 2.281  | 1.239  | 1.304 |

**4 DISCUSSION AND CONCLUSIONS**

The demand for accurate AGB models requires a more thorough understanding of the uncertainties in the input physics which play a role in determining the stellar evolution of AGB stars. Here we present new detailed evolutionary models of two masses, 5 and 6 M⊙, and two metallicities, Z = 0.001 and 0.02. These models are
used to investigate the uncertainties in the stellar evolution when using two differing molecular opacity treatments, $\kappa_C$ and $\kappa_{CO}$, as well as investigating the effects of differing molecular opacity on stellar mass and metallicity. We determine that the AGB lifetime for the lower metallicity models is affected by the choice of the molecular opacity prescription. The increased molecular opacity has the effect of lowering the effective temperature in the low-metallicity AGB models which, in turn, has the consequence of increasing the mass-loss rate. This consequence is confirmed by Marigo (2002) where the increase in the mass-loss rate due to increased molecular opacity serves to better explain the presence of carbon-rich stars in a population of Galactic giant stars. In addition, previous studies by Ventura & Marigo (2009, 2010) highlight the importance of using variable abundance molecular opacities only if the C/O ratio exceeds unity. For low-mass AGB models where HBB does not occur, it is sufficient for the molecular opacity to only follow the increase in carbon due to TDU as with the $\kappa_C$ opacity tables.

Previous studies, such as the stellar models by Karakas et al. (2012), calculate the evolution of intermediate-mass AGB stars using the Mt Stromlo stellar evolutionary code but utilize opacity tables that only account for an increase in carbon due to TDU. This situation has been modelled here using the $\kappa_C$ opacity tables. For the case when the surface C/O ratio does not exceed the initial C/O ratio, the $\kappa_C$ opacity is calculated as if scaled-solar opacity tables had been used. The $\kappa_{CO}$ opacity tables are able to interpolate between lower values, and as a consequence of the decreased opacity the stellar structure is affected. The 6 $M_\odot$, Z = 0.02 model suffers from this omission of lower values below the scaled-solar composition in the low-temperature molecular opacity tables. However, as mentioned by Marigo (2007), the evolution depends on the sensitivity of the mass-loss prescription to the effective temperature.

The studies by Stancliffe, Tout & Pols (2004) and Pignatari et al. (2013, Astrophysical Journal Supplement submitted) calculate $Z = 0.02$ intermediate-mass AGB models which experience efficient TDU. Our study finds that with efficient TDU the surface C/O ratio for the low-metallicity models can exceed unity even with the presence of efficient HBB. The study by Herwig (2004) of $Z = 0.0001$ intermediate-mass AGB models also finds efficient TDU where the C/O ratio exceeds unity for periods of time despite efficient HBB. This is in contrast to Ventura & Marigo (2010), who find a threshold at $M \geq 3.5 M_\odot$ for a metallicity of $Z = 0.001$ where, above this mass limit, the final C/O ratio of the models does not exceed unity. However, the Ventura & Marigo models use an $\alpha$-enhanced composition and this could affect the ability of the models to become carbon rich.

We also investigated the effect of the two different molecular opacity treatments on the stellar yield predictions for 77 species. As illustrated in Fig. 7, the net yields of the low-metallicity models are affected by changes in the stellar evolution due to opacity. The changes in the net yields of the $Z = 0.02$ models are negligible when using the updated $\kappa_{CO}$ opacity treatment. This result indicates the possibility that the changes in yield could be more considerable at a lower metallicity than $Z = 0.001$. The $Z = 0.001$ models of Marigo (2007) utilize synthetic TP-AGB models to investigate the effects of molecular opacity tables. Marigo (2007) concludes that the use of variable molecular opacities should not considerably affect the stellar yields in massive AGB models with $Z \leq 0.001$ as effective temperatures may be so high that the molecules cannot form. We do not find this to be the case for our $Z = 0.001$ models as the effective temperatures are comparable to low-mass AGB models at the same metallicity.

The treatment of molecular opacity along with other input physics such as the choice of the mass-loss rate, reaction rates and treatment of convection all contribute to the uncertainty in AGB models. These uncertainties can have a larger effect at $Z = 0.02$ when compared to the opacity treatment. Ventura & D’Antona (2005a) investigate the effect of the treatment of convection on a 5 $M_\odot$, Z = 0.001 model. They find that the yields strongly depend on the convection model used with significant yield differences between MLT and FST. A previous study on the choice of mass-loss prescription by Stancliffe & Jeffery (2007) finds yield changes of around 15–80 per cent for the light elements when investigating the effect on the yields for a 1.5 $M_\odot$, Z = 0.008 model. These differences are comparable to the results presented in this paper for the Z = 0.001 models. The investigation on mass loss by Karakas et al. (2006) finds yield changes of up to 90 per cent for a 5 $M_\odot$, Z = 0.0001 model. When looking at uncertainties in reaction rates for the Ne–Na and Mg–Al chains, Izzard et al. (2007) find variations of up to two orders of magnitude for some species in the synthetic models. The models of Karakas et al. (2006) find maximum yield differences up to 350 per cent when looking at different $^{22}$Ne + $\alpha$ reaction rates for a 5 $M_\odot$, Z = 0.02 model using the Reimers (1975) mass-loss prescription which is different from that used in this study. The yield differences due to reaction rate uncertainties are significantly higher when compared to uncertainties found here due to the treatment of molecular opacities. Marigo et al. (2013) investigate a number of uncertainties including reaction rates, suppression of TDU and increasing the C and O abundances in the He intershell for a 5 $M_\odot$, Z = 0.001 model. All the models tested become carbon rich and the evolution code is able to accurately follow the surface abundances of C, N and O as the molecular opacity is determined using 'on-the-fly' calculations rather than through the interpolation of tables. The evolution of the surface abundance of a number of light elements as well as the temperature at the base of the convective envelope is shown to be dependent on the tested input parameters. However, with all these sources of inaccuracies, mass loss and convection are thought to dominate the uncertainties in stellar modelling.

One use of stellar models is to provide theoretical predictions of chemical yields for comparison to observational data. Chemical yields are incorporated into chemical evolution models in order to understand the contribution of stellar populations to, for example, the Galaxy or globular clusters (Kobayashi et al. 2011; Cescutti et al. 2012). We have shown that the yields of intermediate-mass AGB stars can be affected by the treatment of molecular opacity in quite a complex way with changes of up to 20 per cent for most isotopes. These results also show that the degree of the difference depends on mass and metallicity. Therefore, it is more suitable to update current stellar models that experience HBB and become carbon rich to include molecular opacity tables that account for the changes in the surface abundances of C and O, as well as N, due to the CNO cycle that occurs during HBB.

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