A Vision for Online Verification-Validation

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Abstract

Today’s programmers face a false choice between creating software that is extensible and software that is correct. Specifically, dynamic languages permit software that is richly extensible (via dynamic code loading, dynamic object extension, and various forms of reflection), and today’s programmers exploit this flexibility to “bring their own language features” to enrich extensible languages (e.g., by using common JavaScript libraries). Meanwhile, such library-based language extensions generally lack enforcement of their abstractions, leading to programming errors that are complex to avoid and predict.

To offer verification for this extensible world, we propose online verification-validation (OVV), which consists of language and VM design that enables a “phaseless” approach to program analysis, in contrast to the standard static-dynamic phase distinction. Phaseless analysis freely interposes abstract interpretation with concrete execution, allowing analyses to use dynamic (concrete) information to prove universal (abstract) properties about future execution.

In this paper, we present a conceptual overview of OVV through a motivating example program that uses a hypothetical database library. We present a generic semantics for OVV, and an extension to this semantics that offers a simple gradual type system for the database library primitives. The result of instantiating this gradual type system in an OVV setting is a checker that can progressively type successive continuations of the program until a continuation is fully verified.

To evaluate the proposed vision of OVV for this example, we implement the VM semantics (in Rust), and show that this design permits progressive typing in this manner.

1. Introduction

We consider the problem of typing unknown, dynamically-determined data obtained from the environment. To illustrate what we mean by unknown, dynamically-determined data, consider the code in Figure 1a that loads a comma-separated value (CSV) file authors.csv using the openDb("authors.csv") call on line 1. The contents of this file are organized into lines, where each line is a row of field values. The first line of the file is special and contains a list of field names instead of field value—see Figure 1b for example content. In line 1 of Figure 1a, the programmer filters the author list down to those that have US citizenship using the field projection author.citizenship.

Suppose the programmer merely wants to know that their code will not access undefined fields—that, in this respect, the program is well-typed. Given that these object fields are defined by the dynamic-generation of data structures via openDb, the validity of this field projection author.citizenship is generally unknowable until after line 1 when the structure of the authors table is defined based on the contents of authors.csv. At the same time, this field projection is clearly valid because of the special first line in specifically this authors.csv shown in Figure 1b.

There is a tension here between static and dynamic checking. On one hand, once the authors table has been determined, the programmer would like the field projections from the rows to be statically verified. But on other hand, how would static checking be feasible if the schema of authors database is dynamically-determined—what would be the type of the openDb function?

To resolve this tension, our key insight is to imagine pausing the concrete execution of Figure 1a right after line 1 and before line 2. Then, imagine reflecting the continuation of the program’s execution to apply abstract interpretation or other static techniques to prove the validity of all subsequent field projections on the rows of the authors table.

Our vision centers around a new paradigm for verification and validation that we call online verification-validation.
(OVV). In contrast to today’s phasic analysis techniques, OVV is phaseless: “static” analysis is freely interposed with “dynamic” execution. By virtue of this mixed approach, OVV transcends the conventional phase distinctions of “static” and “dynamic” analysis. To avoid confusion in this phaseless setting, we refer to static analysis techniques as those for $\forall$-analysis, since they demonstrate universal properties of future program’s states. Likewise, we refer to the techniques used in dynamic analysis as those for $\exists$-analysis, since they demonstrate existential properties about the past program’s states.

In this paper, we make the following contributions:

- We define $\lambda$-VMF, an abstract machine semantics that enables a form of phaseless, online verification-validation (Section 3). The key idea is annotating potentially faulting operations (e.g., field projection) with a certain (!) or uncertain (?) flag, indicating whether or not that operation can be verified. Executing uncertain operations gets stuck, so it is up to the OVV program to progressively rewrite uncertain operations into certain ones by proving the safety of the potentially faulting operation.

- We present a case study of instantiating online verification-validation with a simple, bidirectional gradual type system for dynamic field projection and databases with dynamic schemas (Section 4). The result of instantiating a gradual type system in an online verification-validation setting is a checker that can progressively type successive continuations of the program until a continuation is fully verified (i.e., “statically” typed).

- We implement the proposed design for $\lambda$-VMF in Rust to demonstrate that the proposed instantiating of OVV indeed realizes progressive typing. Our implementation is public: https://github.com/cuplv/vmfuture.

In the next section, we dig deeper into what we term online verification-validation by following the progressive typing of the example program from Figure 1.a.

2. Overview

In Figure 2.a, consider an extension of the example from Figure 1.a with two additional lines. The file books.csv is opened on line 3 and contains a CSV file with book information (shown in Figure 2.b). The final line (line 4) creates a table of books written by US authors, along with the information about those authors.

Observe that this code alternates between dynamically determining the types of the rows and tables (by reading the two files authors.csv and books.csv on lines 1 and 3) and computing over those tables (on lines 2 and 4). This example is a simple version of a pervasive pattern in dynamic languages, where execution interleaves dynamic steps that create new data types (the tables loaded in lines 1 and 3) and steps that compute over previously-defined data types (the filtering and joining steps in lines 2 and 4).

Phaseless Analysis. The essence of online verification-validation is pausing concrete execution to interleave it with abstract interpretation. Pictorially, this interleaving of concrete and abstract execution can be visualized as a two-dimensional grid, as in Figure 3.a. The vertical axis represents the extent of concrete execution and dynamic, $\exists$-analysis (measured by program line), and for each such point, the horizontal axis represents the extent of abstract interpretation and static, $\forall$-analysis performed at this dynamic execution point. As shown, abstract interpretation explores the states after lines 2–4 after pausing at line 1, but revisits the state after line 4 again after pausing at line 3. That is, we imagine suspending the concrete execution of the program in Figure 2.a after the openDb call on line 1 and then interpreting the continuation to statically compute, under an abstraction, the set of reachable future states from this suspended current state (the horizontal axis).

This online look-ahead would permit us to check the projections of author.citizenship and db1[i]["name"] (on lines 2 and 4, respectively) before the running program executes them concretely. However, the other projection in the joinDb call on line 4—the projection of the author field (i.e., db2[j]["author"])—cannot be proven valid in this continua-
tion because the books.csv database has not yet been loaded. But imagine similarly suspending the concrete execution again after line \(3\) (shown as the bottom horizontal execution in Figure 3a). Now in this continuation, an abstract interpretation can easily verify this last remaining projection on all future concrete executions from this point.

For exposition, this example is short, and the distance between the concrete points for static checks and the future concrete points of potential failure (a bad projection) are tiny: they only consist of one or two lines. In the general case, however, the distance between these points can be arbitrarily large. For instance, a long-running scientific workload may last days or weeks, and in these cases, it is critical to know about possible future execution failures as soon as possible, to minimize interruption due to programming errors.

Related Work: Traditional Analyses are Phasic. Typical, existing program analyses impose phase distinctions between static and dynamic steps, forcing each phase to use one approach or the other. At one extreme, today’s techniques for static verification explore all possible execution paths, but have no knowledge of the dynamic execution environment. At the other extreme, dynamic validation explores one path of execution: the path determined by concrete execution.

Type system design is, in general, a tradeoff in checking in an offline, static phase (e.g., are function application expressions well-typed?) and checking in the online, dynamic phase (e.g., is an array-index in bounds?). We illustrate this phasic architecture in Figure 3b where the static and dynamic phases are sequenced and independent.

Some techniques attempt to “blend” these static and dynamic phases, so that information gleaned from one phase feeds into the other. For instance, gradual typing \([35, 36]\) enables shifting type checking between the static and dynamic phases. Or, the notion of using a set of dynamic runs to glean information before static verification appears several times in the literature for call resolution \([13]\), reflection instantiation \([9]\) and for eval \([20, 40]\). We consider such techniques phasic if there is some sequencing (rather than interleaving) of static, \(\forall\)-analysis and dynamic, \(\exists\)-analysis phases.

While phasic analyses dominate the literature, there exist some non-phasic analysis techniques, such as the “proofs-from-tests” approach \([6]\), that mix \(\exists\)-analysis information during \(\forall\)-analysis (e.g., via directed-random automated testing \([22]\)). In these works, the goal is to perform offline static verification whose abstraction selection leverages \(\exists\)-analysis information from testing. This is distinct from our vision, where concrete execution is interposed with analyses (not vice versa). However, this work shares our concern with incremental exploration of a state space, and it possible that our proposed incremental substrate would also be beneficial in the context of “proofs-from-tests.”

```javascript
1  function openDb(file) {
2    var table = openDbInternal(file)
3    {{ reflect/cc (chk_state, return table) }}
4  }
```

Figure 4. The openDb library function synthesizes a type for the loaded table before returning via reflect/cc.

Online Verification-Validation. OVV programs consist of two stratified layers that interact during execution. First, the object layer expresses ordinary execution. Execution can escape into the meta layer, which is capable of inspecting the run-time representation of the object layer. Code at the meta layer expresses \(\forall\)-analysis and \(\exists\)-analysis over object programs. During ordinary execution, the meta layer plays a passive role until special primitives transfer control. In particular, reflect/cc transfers control, along with a reflected view of the current (object layer) continuation. Further, the meta layer has access to read and write hidden annotations on object layer values (e.g., to store program facts, such as types). Collectively, these hidden annotations can be viewed as providing a “shadow heap” for tracking dynamic, meta-level information, in the service of performing \(\exists\)-analyses. For maximum extensibility, the object layer lacks a static type system, relying on checking at the other layer. For convenience in expressing analysis over object programs, the meta layer may employ a language that employs a static type system (a la ML), but this is not a requirement. For concreteness in presentation, we use JavaScript syntax for object layer code and Rust-like syntax for meta layer code, and we may consider language choice as an orthogonal concern.

reflect/cc. The implementor of openDb uses reflect/cc to mediate between concrete execution in the object layer, and interposed code in the meta layer that performs online \(\forall\)-analysis (shown in Figure 4). First, openDb uses openDbInternal to load the given file and construct a table from its CSV content (line 2). Next, line 3 uses reflect/cc to invoke the meta-level function chk_state, which determines types for the table’s content (failing with an error if this content is malformed). As a side effect, it writes to a meta layer field on the table variable to record the type of the rows of the table so that it can be consumed in a subsequent meta layer execution. In particular, the reflect/cc primitive pauses the execution of the object program, giving control to a meta language function, here chk_state. Before transferring control, the primitive reflects the current continuation as a first-class data structure and uses it as an argument to the given meta language code, here chk_state, as we illustrate in Figure 5.

By using this reflected structure, the meta language code can perform arbitrarily complex \(\forall\)-analysis. When it finishes, it returns control to the object program by returning a transformed program state. In this case, openDb uses chk_sstk to type-check the program’s continuation at each call, given
sufficiently powerful to compute meta-theoretical properties to the semantic structures of the object layer, it is meta-level in Rust-like syntax). Because the meta layer has ordinary ML. (The top of Figure 6 defines these structures as values, as if they are persistent (purely this meta-level code interacts with the store typing, stack and VM stack against a store typing and computation type. We Figure 6 lists the meta-layer function \( \text{chk_stk} \) the value has the correct type \( v_t \); and that the stack should contain an argument value with this type. Similar to above, the case checks that the value has the correct type \( v_t \), and checks the stack recursively; when successful, it returns a transformed (annotated) stack.

**Defining and using OVV.** Below, Section 3 defines the syntax and dynamic semantics of \( \lambda \)-VMF in detail; building on these definitions, Section 4 revisits the algorithm shown in Figure 6, showing it in the context of a larger system for gradually-typing programs that compute with databases, like the one shown in Figure 5.

### 3. OVV Machine Semantics

We present \( \lambda \)-VMF, an abstract machine semantics for libraries and programs that employ OVV. In Section 4, we instantiate this OVV framework with a gradual type system for checking programs that compute with simple databases.

**Program Syntax.** Figure 7 gives the syntax for \( \lambda \)-VMF programs. To streamline the definition of analyses and dynamic interpretation, \( \lambda \)-VMF syntactically separates program structure into expressions \( e \) and values \( v \). Further, to permit a meta-layer, extension-defined analysis to annotate \( \lambda \)-VMF programs (as illustrated in Section 4), the recursive syntax of expressions and values consists of annotated pre-expressions \( \hat{e} \) and annotated pre-values \( \hat{v} \), respectively. The

\[
\text{enum Stk} \{ \\
\text{Halt}, \\
\text{FrLet}(\text{Env}, \text{Var}, \text{Exp}, \text{Stk}), \\
\text{FrApp}(\text{Val}, \text{Stk}) \\
\} \\
\text{enum CTyp} \{ \\
\text{Ret}(\text{VTyp}), \\
\text{Arr}(\text{VTyp}, \text{CTyp}) \\
\} \\
\]

\[
\text{meta \text{chk_stk} (st:StTyp, stk:Stk, ct:CTyp)} \rightarrow \text{OptStk} \\
\{ \\
\text{match (ct, stk)} \{ \\
- \text{Halt} \Rightarrow \text{Some(stk)}, \\
\text{Ret(vt)}, \text{FrLet(\text{env}, x, e, stk2)} \Rightarrow \\
\{ \\
\text{match sym_tenv(st, env)} \{ \\
\text{None} \Rightarrow \text{None}, \\
\text{Some(tenv,env2)} \Rightarrow \\
\{ \\
\text{let tenv = tenv_ext(tenv, x, vt)}; \\
\text{match sym_exp(st, tenv, e)} \{ \\
\text{None} \Rightarrow \text{None}, \\
\text{Some(et, e2)} \Rightarrow \\
\{ \\
\text{match \text{chk_stack} (st, stk2, et)} \{ \\
\text{None} \Rightarrow \text{None}, \\
\text{Some(stk3) \Rightarrow Some(FrLet(\text{env2, x, e2, stk3}))} \\
\} \\
\} \\
\} \\
\} \\
\} \\
\text{Arr(vt,ct), FrApp(v,stk2)} \Rightarrow \\
\{ \\
\text{match ( check_value(st, emp, v, vt), \\
\text{check_stack(st, stk, ct))} \{ \\
\text{Some(v3), Some(stk3) \Rightarrow Some(App(v3,stk3))}, \\
\text{- \Rightarrow None,} \\
\} \\
\} \\
\}
\]

**Figure 6.** Type checking continuations.

the type of the loaded table. Based on this type information, openDb either signals errors (if there is a type error), or transforms future validation checks (if type analysis succeeds in proving that these validation checks are redundant).

**The Meta Program Expresses Online Meta Theory.** Figure 6 lists the meta-layer function \( \text{chk_stk} \), which checks a VM stack against a store typing and computation type. We adopt Rust-like syntax (a recent dialect of ML). In particular, this meta-level code interacts with the store typing, stack and computation types as values, as if they are persistent (purely functional, applicative) inductively-defined structures, a la ordinary ML. (The top of Figure 6 defines these structures in Rust-like syntax). Because the meta layer has *meta-level access* to the semantic structures of the object layer, it is sufficiently powerful to compute meta-theoretical properties (either \( \forall \)-analysis or \( \exists \)-analysis). In particular, meta layer function \( \text{chk_stk} \) performs a \( \forall \)-analysis (type-inference and checking), and uses these universal program facts to improve the efficiency of \( \exists \)-analyses that will occur in the future.

At a high level, \( \text{chk_stk} \) traverses the frames of a VM stack (from top to bottom), and checks whether the form of the frame is consistent with the given computation type \( ct \). There are three cases to consider, depending on whether the stack is empty (\( \text{Halt} \)), or has a top-most frame for a \text{let} binding or function application.

The computation type \( \text{Ret}(vt) \) indicates that the local continuation will return a value of type \( vt \), and that the stack should contain a \text{let} body that is expecting to bind this value. The frame \( \text{FrLet(env,x,e)} \) consists of a saved VM environment \( env \) (mapping local variables to values), a variable to let-bind \( x \), and a body \( e \) in which the variable is scoped. To check this case, the code first attempts to synthesize a typing environment from \( env \); if this fails, the stack does not check, and verification fails. Otherwise, the meta-level function \( \text{sym_tenv} \) synthesizes a typing environment and returns an annotated version of the given environment, \( env2 \). Next, the case attempts to synthesize a type \( et \) for the \text{let} body, \( e \). When successful, synthesis produces a type \( et \) and an annotated term \( e \). Finally, the case checks the recursive structure of the stack; when successful, it returns a transformed stack, whose environments, terms and values are annotated.

The computation type \( \text{Arr(vt,ct2)} \) indicates that the local continuation is a function abstraction that will consume a value of type \( vt \), and that the stack should contain an argument value with this type. Similar to above, the case checks that the value has the correct type \( vt \), and checks the stack recursively; when successful, it returns a transformed (annotated) stack.

**Figure 5.** Illustrating online verification-validation.
operational semantics of λ-VMF programs, defined below, does not directly depend on these annotations. However, an extension may use its annotations to prove properties that verify sound online program transformations. In these cases, the annotations can indirectly impact program behavior, i.e., by aiding a meta-level program transformation.

Pre-values consist of open and closed thunks, which represent suspended expressions, including all higher-order data (othunk e and thunk ρ e); closed thunks employ a closing environment ρ that maps the free variables of e to (closed) values. Base types consist of numbers (num n), strings (str s), boolean bits (bool b) and reference cells (loc ℓ). Dictionaries map values to values (dict δ), modeling a row of a database, or a record, where the typical notion of a field name is generalized to any value in λ-VMF.

Pre-expressions consist of forcing a suspended expression (force v), function abstraction (λx.e), function application (e v), let-binding a returned value (let x = e1 in e2), returning a value (ret v), allocating, mutating and accessing mutable storage (ref v, set v1 v2, get v, respectively), updating the field of a record (ext v1 v2 v3), projecting the field of a record (v1 [v2]αβ). Finally, λ-VMF includes special forms for ascribing a sub-expression with a manual annotation (e ?: aα), and reflectively inspecting (and transforming) the current continuation via reflect/cc as core primitive, rcc em e. Notably, execution pauses before executing the local continuation e, and a common idiom consists of using a manual ascription there, to be discharged via the use of rcc.

As explained below, using rcc to prove and discharge ascriptions is actually necessary in λ-VMF, since they have no other form of dynamic semantics. For this purpose, the meta-level program em transforms the program state before its continuation resumes. We do not model the model-level programming language here; our current implementation uses Rust.

VM State syntax. Figure 8 defines the global state of the λ-VMF program: It consists of a store, mapping locations to mutable values (μ), a stack of evaluation context frames (κ), an environment mapping variables to values (ρ), and a pre-expression ℓ that gives the current local continuation. Non-empty stacks give evaluation contexts for let bodies (κ :: (ρ, x, e)) and function application (κ :: v).

Dynamics of λ-VMF Programs. Figure 9 defines a small-step operational semantics over λ-VMF states. The rules for let and function application each push the stack with a frame that is eliminated by the rules for ret and function abstraction, respectively. In both cases, eliminating the frame consists of binding a value to a variable, and continuing the program. Forcing a thunk consists of unpacking its environment and expression, and continuing execution with them. Rules for allocating, mutating and accessing a reference cell in the store are each standard. Dictionary extension adds a field to a (possibly empty) dictionary; and dictionary projection selects a given field’s associated value, returning it.

What makes λ-VMF particularly interesting is that there are no stepping rules for ?-mode field projection or for ascription. To avoid getting stuck at these operations, these operations should be either verified progressively or validated, perhaps immediately before executing, when all relevant information is available. To do so, the program uses rcc em e, which runs the meta-level program em on a reflected version of the current VM state: the rule constructs the current continuation, reflects this program state into a data structure, runs the meta-level term em, and then injects the resulting program state into a transformed continuation σ′. In OVV, this step sometimes verifies and validates operations before the program attempts to execute them, transforming
the program to remove or modify them. In contrast to traditional phasic static verification or dynamic validation (cf. Figure 3), this step does not need to be either eagerly before the entire execution or lazily just before the potentially faulting operation. By choosing the placement of *rcr*, the program can choose how eager or lazy the checking should be anywhere between these two extremes. We give a detailed example below.

4. Gradual Typing for Simple Databases

In this section we present a gradual type system for $\lambda$-VMF and libDb, an extension that permits us to express the motivating example from Figure 2. We tour the type system and illustrate how OVV progressively types and validates the operations in this example.

**Syntax for libDb.** Figure 10 extends the syntax from Figure 7 with the three operations implemented by libDb, for opening databases, filtering them with a predicate, and joining them using named fields. Each operation is parameterized by one or more argument values, and an operation annotation $\alpha^o$ that determines how to type operation. As with record field projection, this annotation determines whether the operation’s pre-conditions for success have been fully verified via OVV. The gradual type system for libDb presented here uses different rules for certain (!) versus uncertain (?) reasoning modes.

**Types for $\lambda$-VMF and libDb.** Figure 11 instantiates the $\lambda$-VMF framework for a gradual type system. This system has (bidirectional, algorithmic) rules to reason about $\lambda$-VMF code as well as the libDb extension. Value types consist of types for thunked computations ($U C$) $\Delta$ dictionaries ($\text{Dict} \, \Delta$, where $\Delta$ maps field values to field types), numbers ($\text{Num}$), strings ($\text{Str}$), booleans ($\text{Bool}$), reference cells ($\text{Ref} \, A$), unit (1), unknown (\?) and databases ($\text{Db} \, A$). Computation types consist of the arrow type for functions ($A \rightarrow C$) and value types for value-producing computations ($F \, A$).

**Typing $\lambda$-VMF program states.** Figure 12 lists typing judgement forms for $\lambda$-VMF program states and for stacks.
State $\sigma$ is well-typed.

\[
\begin{array}{ll}
\text{state} & \frac{|\mu| \vdash \rho \Rightarrow \Gamma}{|\mu|, \Gamma \vdash \hat{e} \Rightarrow C} |\mu| \vdash \kappa \Leftarrow C
\end{array}
\]

Figure 12. Stack typing and State typing

To type a program state, we assume the stored values are annotated, and we use these annotations as a store typing, written $|\mu|$, which maps reference locations to values types. To type a program state, we assume this store typing $|\mu|$ and attempt to verify the the other VM machinery, consisting of the current environment $\rho$, program term $\hat{e}$, and stack $\kappa$. Three judgements compute type properties for these components: Assuming a store typing $\Gamma$, the judgement $\Gamma \vdash \rho \Rightarrow \Gamma'$ computes from an environment (mapping variables to values), a typing context $\Gamma'$ (mapping variables to types). Assuming a typing context $\Gamma$, the judgement $\Gamma \vdash \hat{e} \Rightarrow C$ computes a type from a term $\hat{e}$. Assuming a typing context $\Gamma$ and computation type $C$ for a terminal computation, the judgement $\Gamma \vdash \kappa \Leftarrow C$ checks that the stack $\kappa$ either correctly continues execution or halts.

The remainder of the figure gives three rules for type-checking the stack. First, k-emp says that halting stacks are always permitted. Next, k-let and k-app handle the recursive cases of the stack, where the topmost frame can be viewed as eliminating the terminal computation type, call it $D$. In the case of k-let, we have that $D$ is $FA$, which types the terminal computation that returns a value of type $A$; we check that the top of the stack holds the body of the let, which can use the let-bound variable (of type $A$), for which we can synthesize another computation type $C$ that checks against the rest of the stack. In the case of k-app, we have that $D$ is $A \rightarrow C$, the type of a function abstraction; we check that the top of the stack is an argument value of type $A$, and the rest of the stack checks against the type of the abstraction’s body, $C$.

Transforming $\lambda$-VMF program states. Though the gradual type system defined here is stated propositionally, it constitutes an algorithm, and we demonstrate this fact by implementing these relational definitions as a (mutually) recursive total functions. However, instead of merely returning true or false to indicate the success or failure of the relation to hold, in the case of true, we also construct an annotated term, possibly with transformations (e.g., changing operation annotations from uncertain to certain).

For instance, we implement the type relation for program states as a total function from program states to (optional) program states with annotations; and when the algorithm fails, it returns None. Furthermore, this algorithm plays the role of $\epsilon_m$ in libDb’s use of rcc $\epsilon_m$.

The ability to phrase the typing relations as functional algorithms stems the fact that the rules treat certain positions of their (bidirectional) relations consistently as inputs and outputs, and that outputs are determined functionally from inputs. As an example, Figure 6 gives the algorithmic version of the stack-checking relation $\Gamma \vdash \kappa \Leftarrow C$, which resembles an ordinary function in ML. The remainder of the rules transform in a similar manner, so that checking relations produce an optional, annotated term structure, while synthesizing relations produce an optional pair of annotated term structure and synthesized type. When these functions produce None, the corresponding typing relation is not derivable. The dynamic semantics of $\lambda$-VMF do not permit execution to continue when this occurs.

Typing core $\lambda$-VMF terms bidirectionally. For simplicity, we use a bidirectional type system to encode the gradual type systems of the $\lambda$-VMF core calculus and its libDb extension. Figure 13 defines type checking (above) and synthesis (below) for program terms. For space reasons, we elide some synthesis cases, as well as the checking and synthesis judgements for value forms; the rules shown give a representative flavor for the complete definition.

The analytical (checking) judgement form $\Gamma \vdash e \Leftarrow C$ can be read as, “Under typing context $\Gamma$, term $e$ checks against computation type $C$.” Specifically, the type $C$ is given as an input to the checking judgement, when viewed as an algorithm. The synthesizing judgement form $\Gamma \vdash e \Rightarrow C$ can be read as, “the typing context $\Gamma$ and term $e$ synthesize the computation type $C$.” Specifically, the algorithm computes the type $C$, when given $\Gamma$ and $e$. For the core forms of $\lambda$-VMF, the bidirectional rules for values and computations follow the usual patterns found in bidirectional type systems [10][16]. We show several standard-looking rules, sub, lam, app and annot. In particular, the annotation form of $\lambda$-VMF, $e \vdash a^\alpha$, which asserts the annotation $a^\alpha$ correctly describes the program $e$, plays the role of type ascription in the bidirectional rules; the annot rule says that terms are checked against their type annotations, and these annotated terms synthesize the annotation type. Because it has no dynamic semantics, $\lambda$-VMF uses OVV to prove and discharge this form earlier by rewriting it to $e$ sometime before evaluation; if this rewrite fails, then the program terminates (by failing) early, as a result of OVV failing, not execution.

As is customary in bidirectional systems, type annotations mediate between synthesizing and checking. This provides one the ability to place checking-only terms (such as
Under $\Gamma$, expression $e$ checks against type $C$.

$$\Gamma \vdash e \iff C$$

$$\Gamma \vdash e \Rightarrow C$$

$C \equiv D$ sub

$$\Gamma \vdash e \Rightarrow D$$

$\lambda x. e : A \rightarrow C$ lam

$$\Gamma \vdash \lambda x. e : A ightarrow C$$

Under $\Gamma$, expression $e$ synthesizes type $C$.

$$\Gamma \vdash e \iff C$$

$\Gamma \vdash e ? : C \Rightarrow C$ annot

$$\Gamma \vdash e \Rightarrow A \rightarrow C$$

$$\Gamma \vdash e \Rightarrow C$$

$$\Gamma \vdash e \Rightarrow C$$

$$\Gamma \vdash e \Rightarrow C$$

Gradual typing for dictionary projection. The typing rules for uncertain and certain projection differ in what is known about the record and field values, and illustrate a form of gradual typing. In the uncertain case, rule $p\ ?$ synthesizes return type $?$, since nothing is known about the dictionary of values being projected. By contrast, in the certain case, the dictionary type is known to rule $p!$, and this dictionary maps the given field value to a corresponding field type. In this case, the soundness of the type system means that the projection must succeed in all possible future program states, and moreover, that the projected value has the given type.

Typing the $libDb$ operations. The rule openDb? is uncertain and has no certain counterpart: The type of the database is not known until after the operation completes, just before execution resumes with its continuation; before then, the database could hold any type, so the rule types the returned database as $Db \ ?$.

Following similar reasoning, since filtering and joining databases occur after a database is loaded, it is possible to type these operations in both uncertain and certain modes. The rule filterDb? says that filtering a database of uncertain values leads to another database of values with an uncertain type; since it merely assumes the type of the database is $?$, it does not prove that the predicate will not “go wrong”, e.g., by projecting the wrong field from its argument. By contrast, the rule filterDb! says that filtering a database of known type using a predicate that checks against this type leads to a database with the same known type; in this case, the soundness of the type system means that the predicate must always succeed.

Similarly, the rules for joinDb? and joinDb! follow the pattern set above: the uncertain rule assumes nothing about the argument values, beyond the arguments actually consisting of databases. The certain rule assumes that the database arguments’ types are fully known, that the chosen field values are mapped in these types, and that the chosen fields share a common type (we want to compare values of this field for equality to perform the join).

Gradual Typing, Progressively via $OVV$. Figure 14 illustrates using the typing rules of Figure 13 to perform gradual typing our four-line motivating example (Figure 2a). The vertical and horizontal dimensions of the table list each of the four lines; the vertical axis represents concrete ex-
execution, and the horizontal axis represents typing the four right-hand-sides of the program’s four let-bindings, and in particular, for filterDb (on Line 2) and joinDb (on Line 4), the table indicates whether the operation was typed in the uncertain or certain modality. As execution progresses (vertically) over Lines 1 and 3, the typing of the program continuation’s becomes more certain: After Line 1 executes, Line 2 types in the certain modality (!) instead of the uncertain modality (?); similarly, after Line 3, Lines 4 onward type using the certain modality. As the final column shows, the certainty of code using these tables in the remainder of the program (Line 5 onwards) increases after each of the two calls to openDb. Between the two calls, some information is known (relating to the first two tables defined on Lines 1 and 2), but some information is still missing (relating to the two tables defined in Lines 3 and 4).

Our current Rust-based prototype of λ-VMF is powerful enough to express this example, including the progressive typing discussed above. In Section 5, we discuss the potential to use incremental computation in the context of such progressive typing; the goal is to improve performance by exploiting the redundancy of re-typing the program’s continuation.

5. Discussion

In this section, we discuss future challenges and directions for the vision of OVV presented in this paper. Specifically, we discuss the design of the meta- and object-level programming languages, and their use in expressing progressive verification and regressive validation.

Incremental Computation for Progressive Verification. In the motivating example from Section 2, the chk_stk calls performed by openDb use progressive typing to check their continuations. In fact, these two continuations are related: The earlier version lacks type information about the table loaded in line 3, whereas the later version has access to this type information. Progressive typing could exploit this incremental relationship to avoid re-computing all of the typing facts about the program state that have not changed.

Progressive typing is a specific instance of progressive verification. Pictorially, progressive verification relates distinct abstract executions (shown horizontally in Figure 15a), by exploiting their similarity (a small change, depicted as δ, extending vertically). The task of a progressive verifier is a ∀-analysis, just like a classical static verifier, which attempts to prove that all executions to an assertion satisfy a particular safety property.

More Aggressive Regressive Validation. After type checking the continuation for line 1, regressive validation consists of eliminating dynamic checks within the library calls of lines 2 and 4 (filterDb and joinDb, respectively). In particular, if the continuation type-checks under the partially-known type information, the known type information can be used to elide run-time ∃-analysis checks that concern the authors table, including the asserts for the projections of author_name. Pictorially, we think of regressive validation as introducing a third dimension that consists of all possible outcomes of a program transformation on the object program (shown in Figure 15b). After performing an online verification, the meta layer transforms the continuation, either eliding certain downstream validation checks (labeled validate), or introducing residual checks that reduce the original checks’ complexity (labeled residual). As illustrated in Section 4, progressive typing can, before executing the operation, eliminate residual checks by rewriting uncertain operations to certain operations (which require no run-time type checks). More aggressive verification techniques can hope to regress even more aggressive validation checks to simpler forms. For instance, global heap-based properties present an interesting challenge.

Implicitly-Incremental Meta-Level Computation. In sum, the example chk_stk above encodes a theory about online typing, along with a mechanism for using this type information to optimize the dynamic run-time checks that would otherwise be used. The meta layer should have an in-built ability to implicitly express progressive verification as ordinary verification, so that the system, not the programmer, takes into account execution environment changes across these progressive stages. Further, when the meta layer uses this progressive verification to enable regressive validation in the future execution down stream, the system, not the programmer, accounts for these changes when doing future stages of progressive verification. In other words, the VM that runs the meta language and object language should have an in-built ability to express interaction among the levels in terms of implicitly-incremental computation. In Section 6, we discuss the challenges that OVV poses to work on general-purpose incremental computation.
6. Related Work

This section supplements the related work in Section 2.

General-Purpose Incremental Computation. Section 5 proposes an implicitly incremental meta-level language for \(\lambda\)-VMF, which challenges current research on (general-purpose, programming language-based) incremental computation (IC). Consider the desired incremental behavior of \(\text{chk}_{\text{stk}}\) in the motivating example, where it occurs after lines 1 and 3, when the program states are similar, but not identical. In particular, both continuations include the AST of the call in line 4, and onward, which \(\text{chk}_{\text{stk}}\) will process in both verification stages. The central challenge is reusing the redundant work performed by \(\text{chk}_{\text{stk}}\), despite the fact that the AST and store typing are not equal to that in the prior stage, which creates challenges for incremental computing via memoization, a key implementation mechanism used across many specific IC approaches.

To understand why these “small” changes are challenging for typical memoization, consider the structural recursion of the \(\text{chk}_{\text{stk}}\) function from Figure 6. One approach to memoization identifies each saved invocation by the entire store typing \(\sigma_t\) and entire stack \(\text{stk}\), including all of their recursive sub-structure, e.g., via hash-consing [18]. This approach is commonly taken by past work on incremental computation [7] [8] [17] [23] [24] [32] [33], however, it is brittle and overly sensitive to small changes, since they alter the identity of the whole recursive structure. Recent work addresses this shortcoming by introducing unique names that are special to incremental computing [25]. This naming mechanism can overcome the challenges outlined above for \(\text{chk}_{\text{stk}}\), since the presence of names isolates changed components of the store typing, stack and local environments.

However, several key challenges remain before these techniques can fully realize OVV: We want to use these names correctly (to avoid unsound incremental results), use them efficiently (to isolate changes and avoid sub-redundant computations) and use them implicitly (so that the meta-level programs look like ML). Further, we may want to control how fine-grained the IC techniques track program dependencies, to reduce constant-factor overhead.

Reflective Towers of Interpreters. As proposed in Section 5, future work on \(\lambda\)-VMF should permit library extension authors to write meta programs and object programs in an integrated way. Fortunately, many researchers have proposed designs that allow interesting interplay between the interpreter’s viewpoint (where the meta-level program runs) and the program being interpreted (where the object program runs). Conceptually, this work begins with 3-LISP [14] [37], which gives the programmer access to an infinite tower of (so-called meta-circular) interpreters, allowing them to redefine the language from within the language. Following (theoretical) work on 3-LISP, researchers give various approaches that attack practical concerns in how to express and implement reflective towers in simpler terms; these efforts are named after various hair colors: Brown [19] [39], Blond [13] and most recently, Black [3] [4].

Compared to the impressive and mind-bending work on metacircular interpreters, the vision for \(\lambda\)-VMF is more modest: Two levels suffice to perform OVV. Having said that, if meta-level programmers want to verify their metalevel programs as object programs (to “bootstrap” a typed meta level), the work mentioned above will likely provide further insights.

Program Analysis for Dynamic Languages. The ultimate aim of online verification-validation is offer “strong checking” in an extensible, dynamic language environment. And thus we seek to build on the substantial amount of research activity on program analysis for dynamic languages. Since by definition, dynamic languages lack a built-in static typing discipline, much of the static verification work focuses on either retrofitting rich typing or specification disciplines [11] [12] [21] or applying whole-program flow analysis for inferring and checking type properties (e.g., for JavaScript [5] [26] [27] or for Ruby [11]).

The dynamic language features that make widely-used libraries like jQuery possible also make retrofitting static techniques incredibly challenging [2] [28] [34] [38]. Much of this work focuses on finding the right kinds of context-sensitivity to try to more precisely resolve the flow of values to dynamic features like dynamic property read in a static analysis [2] [31] [38] or to determine when dynamically-observed information is sufficient to apply in a static verification [34]. We expect such techniques to be not only applicable and useful but strengthened in an OVV context. In the end, static techniques in a phasic setting are limited by what is indeed available statically, and dynamic techniques are limited by what can be observed in testing runs. As exhibited in Section 2, the vision of OVV enables these techniques to be strengthened with a flexible interleaving of “static” and “dynamic” analysis (i.e., \(\forall\)-analysis and \(\exists\)-analysis).

7. Conclusion

This paper presents a vision for online verification-validation (OVV), an approach to ease the tension between extensibility (of dynamic languages) and safety (of static languages). The key insight of OVV is that analysis in a VM can be phaseless, allowing analyses to run progressively on the object program by pausing execution, reflecting on the current continuation, and transforming the continuation to replace uncertain (?) operations with certain (\(\exists\)) ones.

In this paper, we formalize an approach for OVV as a language semantics and Rust-based implementation called \(\lambda\)-VMF. We explore a proof-of-concept instantiation of OVV by defining a gradual type system for dynamic field projection and databases with dynamic schemas, and we observed that the result is a progressive type checker.
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