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Effect of TiO$_2$ Nanoparticles on Capillary-Driven Flow in Water Nanofilters Based on Chitosan Cellulose and Polyvinylidene Fluoride Nanocomposites: A Theoretical Study

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1. Introduction

The occurrence of micro-sized particle wastes such as heavy metals, microplastics, and pathogens in drinking water presents great risks for human health and biodiversity. Recently, Darren et al. performed water chemistry analysis and size fractionation sampling of drinking water at four houses in the city of Newark, New Jersey [1]. They found the existence of pyromorphite (Pb$_5$(PO$_4$)$_3$Cl) microparticles with size < 100 nm in drinking...
water samples that passed through the tap or pitcher filtration units. Barbara et al. investigated 32 water bottle samples from 21 different brands of mineral water from Bavarian food stores [2]. They detected variable amounts of microsized plastics and pigments in both reusable and glass bottles. They ascribe their occurrence and possible contamination to various sources, such as from the washing machinery, the bottle cap, and other steps during the filling process. Additionally, other sources of drinking water (e.g., surface water, groundwater) are likely to be polluted by microparticle wastes such as heavy metals, pathogens, and pesticides [3–5].

Regarding this state-of-the-art, a supplementary domestic filtration process is an adequate solution for purification of the tap and bottled drinking water. Lately, a considerable literature has developed around the theme of the purification of drinking water from the nano- and micro-sized particles using reverse osmosis (RO), nanofiltration (NF), chemical coagulation, adsorption, and magnetic nanoparticles processes [6–12]. Typically, the Nanofiltration (NF) process is the suitable domestic purification process for tap and bottled drinking water. In fact, NF has greater flux and less energy use rates, operational under normal conditions, and its unique advantages of retaining at an optimum the essential multivalent and all monovalent minerals ions required for the human body [6,7,13,14]. However, the main common disadvantages of the previous processes are their energy consumption, removing all minerals essential ions required for human body (RO), and more difficult installation as a domestic purification solution. Moreover, the NF process commonly introduces supplementary pressure to drive water inside the nanopores and to increase the permeation rate of the nanofilter membranes, which leads to an increase in their cost-effectiveness [15,16].

Very recently, emerging studies focused on exploring the so-called capillary-driven nanofiltration process as a natural, free energy, and sustainable process for water purification [17–20]. This ubiquitous nanofiltration natural process allows water transport throughout nanoporous materials only using capillary pressure and without the help of external forces [19,20]. In fact, at the nanoscale, the flow of the water inside the nanoporous structure, known as imbibition, is driven by the capillary pressure. For hydrophobic materials, the capillary pressure tends to pull water from the nanopores. The reason for that is the nanofilter based on hydrophobic materials requires supplementary pressure driven to overcome the capillary pressure and to drive water inside the nanopores [21]. This fact may cause membrane destruction and then increase the cost-effectiveness of the NF process and loss in purification efficiency of the nanofilter membranes [15,16]. For hydrophilic materials, the water flows spontaneously throughout the nanostructure due to the capillary pressure and then generates a natural flow through the nanofilter without any additional pressure [17–20].

For instance, there are poor attempts to implant the capillary-driven nanofiltration using bio-based materials as a free energy, biocompatible, and sustainable solution for the purification of drinking water.

Therefore, the purpose of this study is to demonstrate how to develop a capillary-driven NF on bio-based porous nanocomposites as a newly sustainable domestic purification process of tap and bottled drinking water with zero energy consumption. To do so, it is essential to study quantitatively and qualitatively the effect nanofilter materials composition have on their wettability as well as their water permeability in terms of capillary-driven flow.

Actually, an emerging trend is underway to develop novel synthetic and biodegradable nanocomposite polymers for use in the NF process [22–26]. They suggest the incorporation of NPs-based metal oxides materials for increasing water permeability, mechanical strength, separation efficiency, and reducing fouling of the membrane [27–29].

In this paper, we aim to give a detailed theoretical investigation of the effect of NPs filling rates on the physical properties that involves the spontaneous capillary-driven NF: the surface energy, wettability, capillary pressure, and capillary-driven water volume for some biodegradable and synthetic nanocomposites commonly used as nanofilters for drinking water.
Titanium dioxide (TiO$_2$) NPs was chosen as filler for the nanocomposites because of their prominent properties such as abundance in nature, biocompatibility, low-cost preparation with different sized and shaped particles (including nanowires, nanotubes, nanofibers, core-shell structures, and hollow nanostructures), and antiseptic and antibacterial properties [30]. Chitosan (CS) and cellulose acetate (CLA) were chosen as bio-based and biodegradable polymer matrix, whereas polyvinylidene fluoride (PVDF) was chosen as synthetic non-biodegradable polymer [31–33].

The following part of this study is dedicated to the presentation of the theoretical methods used for the evaluation of the surface energy, water contact angle, capillary pressure, and the capillary-driven water volume as function of the TiO$_2$ NPs volume fraction. In the next section, we demonstrate that the pure polymer matrix exhibits a hydrophobic behavior, which leads to negative capillary pressure around the nanopores, that acts as draining force of water from the nanopores of the nanofilter and, therefore, prevents the capillary-driven NF process. Afterwards, the threshold filler rate of TiO$_2$ NPs required to activate capillary-driven flow is determined for each polymer’s nanocomposite. Later, the enhancement of water flow throughout the nanocomposite’s nanofilters in terms of capillary rise and capillary-driven water volume will be demonstrated by increasing the volume fraction of the TiO$_2$ NPs. At the end, using a recapitulative comparison study, we demonstrate that the nanofilter based on biodegradable CS/TiO$_2$ and CLA/TiO$_2$ nanocomposites provides better capillary-driven NF performance than the synthetic nanocomposites PVDF/TiO$_2$ one.

2. Materials and Methods
2.1. Capillary Nanofiltration
2.1.1. Nanofiltration and Capillary Pressure

NF is purification process based on the flow of water through nanopores/nanochannel sizes from 1 to 10 nm for the removal of waste microparticles that have a diameter larger than the nanopores of the membrane [34]. Figure 1 shows a brief description of the principle of capillary-driven NF proposed in this study. The flow of water on both sides, superior and inferior, of the membrane is governed by gravity (from top to bottom). However, the flow of water throughout the NF membrane is driven by action of capillary pressure which depends on the wettability [17,35].

![Figure 1](image)

In fact, at normal conditions of temperature and pressure, the spontaneous flow of the water across porous structure is determined by an interplay of surface and gravity forces. The influence of the gravity force on the flow of water inside nanopore can be found by calculation of the so-called capillary length of water [36]:

$$\lambda_c = \sqrt{\frac{\gamma}{\rho g}}$$

Figure 1. Schematic illustration of capillary-driven NF principle for $r_p << \lambda_c$. 

Finally, the spontaneous flow of the water across porous structure is determined by an interplay of surface and gravity forces.
where $\gamma$ and $\rho$ are surface tension and the density of water and $g$ is the acceleration of the gravity. For water (with $\gamma = 72 \times 10^{-3}$ N·m$^{-1}$ and $\rho = 1000$ kg·m$^{-3}$). Equation (1) yields a capillary length of water equal to 2.7 mm.

Usually, for surfaces with characteristic lengths smaller than $\lambda_c$, the gravitational force can be neglected. Therefore, for nanofilter membrane with pore radius ranges from 1 nm to 10 nm, we have $r_p \ll \lambda_c$ and then the influence of the gravity force in water flow is ignored. Consequently, the flow of water throughout the nanofilter membrane is a function of surface forces i.e., wettability and capillary pressure.

As presented in Figure 1, for the hydrophilic nanofilter membrane, the transport phenomenon of water throughout the nanopores is governed by so-called capillary-driven flow, whereas for a hydrophobic nanofilter membrane, the capillary forces pull water from the nanopore and this results in the drainage of water.

To evaluate the strength of the capillary pressure, we use the Young–Laplace equation, which relies on the capillary pressure to the contact angle of water $\theta$, the surface tension of water $\gamma_l$, and the capillary pore radius $r_p$ by [37]:

$$P_c = P_{nw} - P_w = \frac{2\gamma_l \cos \theta}{r_p}$$  \hspace{1cm} (2)

The capillary pressure ($P_c$) acts as the difference between pressure non-wetting ($P_{nw}$) and wetting ($P_w$) phases.

As shown in Figure 2a, at the interface water–membrane–air, when the adhesion force (i.e., force with which water molecules adhere to a membrane surface) is less than the cohesion force of water molecules, the water does not penetrate spontaneously into nanopores and it forms a convex meniscus with contact angle above $\theta > 90^\circ$.

Figure 2. Capillary pressure action in nanopore $r_p \ll \lambda_c$ (a) capillary filling with hydrophilic nanocomposite (b) capillary draining with hydrophobic nanocomposite.

However, when the force of adhesion is greater than the cohesion force of water molecules and it forms a concave meniscus with contact angle less than $90^\circ$ (Figure 2b), water molecules tend to penetrate spontaneously into nanopores [38]. This latter situation is defined as the capillary-driven flow known as spontaneous imbibition [17–19,35].

2.1.2. Capillary Rise in Nanopore

Capillary rise is defined as the movement of water within porous materials due to the forces of adhesion, cohesion, and surface tension. In this study, we consider a straight nanopore of radius $r_p \ll \lambda_c$ in contact with water of viscosity $\mu$. For $\theta < 90^\circ$, the water is pulled inside the nanopore by the net interfacial force $2\pi r_p \gamma \cos \theta$. At the equilibrium,
the final capillary rise \( y_f \) is determined by the force balance between the capillary force \( f_c = 2\pi r_p \gamma \cos \theta \) and the gravity force \( f_g = \rho g \pi r_p^2 y_f \) known as Jurin’s law [38]:

\[
y_f = \frac{2\gamma_\text{l} \cos \theta}{\rho g r_p}
\]  

(3)

When \( y \) is much smaller than \( y_f \), the capillary force \( f_c \) and viscous friction force \( f_f = \mu V \cdot y \) become the two driven forces which govern the flow of the water. This is the so-called viscous regime in which the capillary rise \( y \) as function of time \( t \) is described by Washburn’s law [39]:

\[
y(t) = \sqrt{\frac{r_p \gamma_\text{l} \cos \theta}{2\mu t}}
\]  

(4)

2.1.3. Modified Lucas–Washburn for Predicting Capillary-Driven Water Volume

To take account of the morphological characteristics of nanoporous medium on capillary filling kinetics, Benavente et al. [40] developed the Lucas–Washburn (LW) model for predicting the capillary-driven liquid volume \( V \) over time \( t \) throughout nanoporous material, which is related to the capillary rise as in the following equation:

\[
V(t) = S \cdot \phi \sqrt{\frac{\delta}{\tau}} y(t) = S \cdot \phi \sqrt{\frac{\delta \gamma_\text{l} \cos \theta}{2\mu \tau}} t
\]  

(5)

where \( S \) is the cross section of the nanofilter surface, \( \phi \) is the porosity of the nanofilter membrane, \( \delta \) is the pore shape factor (\( \delta = 1 \) when the cross section of the pore is a perfect circle), \( \tau \) is the correction factor of tortuosity (equal 1 to the straight pore channel and \( 1 < \tau < 3 \) for random pore channels).

The tortuosity is directly related to the porosity within the classical fluid flow approach [41] as in the following equation:

\[
\tau = 1 - 0.77 \ln(\phi)
\]  

(6)

2.1.4. Wettability: Contact Angle and Surface Energy

Wettability plays a crucial role in determining water permeability of porous membrane. It is well-known that hydrophilic porous materials exhibit a higher permeability than hydrophobic ones [17]. According to relation 2, this evidence can be understood in terms of capillary pressure. In fact, the capillary pressure is positive (filling action) for hydrophilic materials and negative (draining action) for hydrophobic.

- Contact angle

According to Young’s equation, the contact angle \( \theta \) (Figure 2) results from the thermodynamic equilibrium between the surface tension of water \( \gamma_\text{l} \), the interfacial tension water/nanocomposite \( \gamma_{\text{sl}} \), and the surface energy of the nanocomposites \( \gamma_s \) as [42]:

\[
\cos \theta = \frac{\gamma_s - \gamma_{\text{sl}}}{\gamma_\text{l}}
\]  

(7)

where \( \gamma_{\text{sl}} \) is determined by [43] (p. 417):

\[
\gamma_{\text{sl}} = \gamma_s + \gamma_1 - 2\sqrt{\gamma_1^D \gamma_s^D + \gamma_1^P \gamma_s^P}
\]  

(8)

where \( \gamma^D \) and \( \gamma^P \) denote the dispersive and polar component of surface energy.

- Surface energy
To evaluate the surface energy of nanocomposites as a function of the TiO$_2$ NPs volume fraction, we used a theoretical method that allowed calculating the surface energy from the evaluation of the Hamaker constant as in the following equation [43] (p. 415):

$$\gamma = \frac{H}{24 \cdot \pi \cdot x_0^2}$$  \hspace{1cm} (9)

where $x_0$ the interatomic distance between two surfaces in contact called the cut-off distance typically equals to 0.165 nm and $H$ is the Hamaker constant.

2.2. Method for Calculation of the Hamaker Constant

The Hamaker constant $H$ is a fundamental constant for describing qualitatively and quantitatively the van der Waals (vdW) intermolecular interaction that governs the surface forces. On the basis of the Lifshitz theory, the Hamaker constant is a function of the bulk properties of the interacting mediums: their dielectric constants $\varepsilon$, and their refractive indexes $n$ [43] (p. 260):

$$H = H^P + H^D$$  \hspace{1cm} (10)

where $H^P$ is the polar part of the Hamaker constant. It regroups the Keesom interaction that arises from permanent molecular dipoles and the Debye interaction that arises from permanent dipoles and induced dipoles [44,45]. It is expressed as a function as dielectric permittivity as in the following equation [43] (p. 260):

$$H^P = \frac{3}{4} k_B T \left( \frac{\varepsilon_1 - \varepsilon_2}{\varepsilon_1 + \varepsilon_2} \right)^2$$  \hspace{1cm} (11)

where $k_B$ is the Boltzmann constant, $T$ is the temperature, ($\varepsilon_1$, $\varepsilon_2$) are, respectively, the dielectric permittivity of the nanocomposite and air.

However, $H^D$ is the dispersive part of the Hamaker constant that regroups the London van der Waals forces resulting from the fluctuations in the charge densities of the electron clouds surrounding the nuclei of the atoms [46]. It is expressed as function of the refractive index of the three interacting mediums and it is given by the following equation [43] (p. 260):

$$H^D = \frac{3h \nu_e}{16 \sqrt{2}} \left( \frac{n_1^2 - n_2^2}{n_1^2 + n_2^2} \right)$$  \hspace{1cm} (12)

$\nu_e$ is the main electronic absorption frequency in the UV typically around $3 \times 10^{15}$ s$^{-1}$ [43] (p. 260), $h$ is the Planck constant, and ($n_1$, $n_2$) are, respectively, the refractive index of nanocomposite and air in the visible spectrum (at 600 nm).

2.3. Model for Calculation the Dielectric Constant of Nanocomposites

The power-law model is used to calculate the dielectric constant as a function of the volume fraction ($\phi$) of the NPs filler added to the nanocomposites. Hypothetically, we consider that the NPs filler have a spherical form and they are uniformly dispersed in the continuous polymer matrix [47]:

$$\varepsilon_1^{1/3} = \Phi \varepsilon_m^{1/3} + (1 - \Phi) \varepsilon_i^{1/3}$$  \hspace{1cm} (13)

2.4. Models for Calculation of the Refractive Index

The refractive index of the nanocomposites is calculated using the popular mixing theory of Maxwell garnet [48]:

$$n_c^2 = n_m^2 \left( \frac{n_i^2 + 2n_m^2}{n_i^2 + 2n_m^2} + 2\Phi(n_i^2 - n_m^2) \right) \left( \frac{n_i^2 + 2n_m^2}{n_i^2 + 2n_m^2 - \Phi(n_i^2 - n_m^2)} \right)$$  \hspace{1cm} (14)
where $\Phi$ is the volume fraction of NPs filler, $n_c$, $n_m$ and $n_f$ are the refractive indexes, respectively, of nanocomposites, polymer matrix, and TiO$_2$ NPs filler.

The method and models used in this study for evaluation of the surface energy have been validated by many pertinent research studies [43] (p. 278), [49–52].

2.5. Materials

The material chosen in this study are from two categories. Chitosan (CS) and cellulose acetate (CLA) were chosen as the bio-based and biodegradable polymer matrix. Whereas, polyvinylidene fluoride (PVDF) was chosen as synthetic polymer. These polymers have facilitated a great interest in drinking water and wastewater treatment using many processes, such as adsorption, NF, and reverse osmosis [22–29]. Their main advantageous properties are abundance, chemical stability in aqueous medium, mechanical strength, and cost-effectiveness [53–55].

However, TiO$_2$ anatase NPs were chosen as filler to these polymer matrices. Moreover, their common advantages with the polymer matrix, TiO$_2$ NPs, provide many prominent properties for water treatment, such as biocompatibility, antibacterial, and good photostability [56,57].

Actually, there are many easy and ecofriendly techniques for manufacturing nanocomposites nanofilter membrane for water purification, such as the phase inversion process, thermally induced phase separation, chemical bond connection, and interfacial polymerization [58–60].

Hereafter, the volume fraction rates of TiO$_2$ NPs added to CS, CLA and PVDF polymer matrix are fixed to 0%, 10%, 20%, and 30%, and they are designated in the study as presented in Table 1.

Table 1. Affected names of CS, CLA, and PVDF filled TiO$_2$ NPs nanocomposites.

| $\Phi$ % of TiO$_2$ NPs | Nanocomposite          |
|-------------------------|------------------------|
|                         | CS/TiO$_2$ | CLA/TiO$_2$ | PVDF/TiO$_2$ |
| 0                       | CS         | CLA         | PVDF        |
| 10                      | CS/TiO$_2$-10 | CLA/TiO$_2$-10 | PVDF/TiO$_2$-10 |
| 20                      | CS/TiO$_2$-20 | CLA/TiO$_2$-20 | PVDF/TiO$_2$-20 |
| 30                      | CS/TiO$_2$-30 | CLA/TiO$_2$-30 | PVDF/TiO$_2$-30 |

In Table 2, we summarized the dielectric constant and the refractive index of the materials for the calculation of the Hamaker constants.

Table 2. Dielectric constants and refractive indexes of polymers matrixes, TiO$_2$ NPs filler, water, and air at room temperature (298.15 K).

| Material      | $\varepsilon$ at 1 MHz | $n$ at 600 nm |
|---------------|------------------------|---------------|
| Bio-based polymer | CS                     | 5.5 [61]     | 1.53 [62]  |
|                | CLA                    | 5 [63]       | 1.47 [64]  |
| Synthetic polymer | PVDF                  | 8.5 [65]     | 1.42 [66]  |
| Filler        | TiO$_2$ (Anatase)     | 86 [67]      | 2.60 [67]  |
| Air           |                        | 1 [43]       | 1 [43]     |
| Water         |                        | 78.4 [68]    | 1.33 [68]  |

3. Results and Discussion

All the calculations and the discussions of the results were made at standard temperature ($T = 25$ °C = 298.15 K) and pressure ($P = 1$ atm = 101.325 kPa).

3.1. Effect of TiO$_2$ NPs Filling on Surface Energy

We can deduce from relation 2 the capillary pressure is function of the contact angle, the surface tension of water, and pore radius. Hence, we report the variation in the contact
angle by varying the surface energy of nanocomposites during filling with TiO$_2$ NPs and nanopore radius (1 to 10 nm), while the surface tension of water is always constant ($\gamma_l = 72 \times 10^{-3}$ J m$^{-2}$).

Table 3 shows an increase of the refractive index and the dielectric constant of all nanocomposites after incorporation TiO$_2$ NPs filler. This raise is attributed to the elevated refractive index and dielectric constant of TiO$_2$ NPs compared to those for the pure CS, CLA, and PVDF polymer matrixes.

### Table 3. Refractive index and dielectric constant of CS/TiO$_2$, CLA/TiO$_2$ and PVDF/TiO$_2$ nanocomposites as function of volume fraction of TiO$_2$ NPs.

| $\Phi$% (TiO$_2$) | n  | CLA/TiO$_2$ | PVDF/TiO$_2$ | n  | CLA/TiO$_2$ | PVDF/TiO$_2$ |
|------------------|----|-------------|--------------|----|-------------|--------------|
| 0                | 1.53 | 1.47       | 1.42         | 5.5   | 5           | 8.5          |
| 10               | 1.61 | 1.56       | 1.51         | 8.36  | 7.76        | 11.82        |
| 20               | 1.70 | 1.65       | 1.61         | 12.08 | 11.40       | 15.91        |
| 30               | 1.80 | 1.75       | 1.70         | 16.77 | 16.02       | 20.86        |

Table 4 reports the Hamaker constants calculated from relations (10-11-12). It is apparent from this table that the Hamaker constants for the system nanocomposite–air are still positive and in the range of $\times 10^{-20}$ J [43] (p. 261). Interestingly, this suggests the preciseness of our used model for computing of the vdW intermolecular interactions that governs surface forces [43] (pp. 253–289).

### Table 4. Hamaker constants of CS/TiO$_2$, CLA/TiO$_2$ and PVDF/TiO$_2$ nanocomposites as function of volume fraction of TiO$_2$ NPs.

| $\Phi$% (TiO$_2$) | H$^P$ (10$^{-21}$ J) | H$^D$ (10$^{-20}$ J) | H (10$^{-20}$ J) | H$^P$ (10$^{-21}$ J) | H$^D$ (10$^{-20}$ J) | H (10$^{-20}$ J) |
|------------------|---------------------|---------------------|-----------------|---------------------|---------------------|-----------------|
| 0                | 2.08                | 5.11                | 5.325           | 2.00                | 4.62                | 4.82            |
| 10               | 2.36                | 5.81                | 6.049           | 2.32                | 5.36                | 5.59            |
| 20               | 2.54                | 6.48                | 6.738           | 2.52                | 6.09                | 6.34            |
| 30               | 2.670               | 7.13                | 7.399           | 2.65                | 6.78                | 7.04            |

After providing the Hamaker constant, the surface energy is then calculated using Equation (9). As it can be observed in Tables 5 and 6, for purely CS, CLA, and PVDF polymer matrixes, the surface energy range values ($20–43 \times 10^{-3}$ J m$^{-2}$) are in good agreement with those reported by many studies (Table 6), which confirms the accuracy of our used model for the evaluation of the surface energy.

### Table 5. Surface energy of CS/TiO$_2$, CLA/TiO$_2$ and PVDF/TiO$_2$ nanocomposites as function of volume fraction of TiO$_2$ NPs.

| $\Phi$% (TiO$_2$) | CS/TiO$_2$ | CLA/TiO$_2$ | PVDF/TiO$_2$ |
|------------------|------------|-------------|--------------|
|                  | $\gamma_s^P$ (10$^{-3}$ J m$^{-2}$) | $\gamma_s^D$ (10$^{-3}$ J m$^{-2}$) | $\gamma_s$ (10$^{-3}$ J m$^{-2}$) |
| 0                | 0.72       | 37.82       | 38.54        |
| 10               | 0.93       | 48.91       | 49.84        |
| 20               | 1.08       | 61.04       | 62.12        |
| 30               | 1.18       | 74.15       | 75.33        |

However, in accordance with our earlier observations on the Hamaker constant, the surface energy was, remarkably, increasing with filler rates ($\Phi = 10\%$, 20% and 30%) of TiO$_2$ NPs for all nanocomposites. This increase was significantly important in the order PVDF/TiO$_2 < CLA/TiO_2 < CS/TiO_2$. Therefore, it is well-known that the incorporation
of TiO2 NPs give rise to an increase of the dispersion and polar vdW intermolecular interactions that governs surface forces of the nanocomposites.

Table 6. Surface energy of CS, CLA and PVDF polymer matrixes provided by this study and from literature.

| Polymer | $\gamma_s$ $(10^{-3}$ J m$^{-2}$) |
|---------|----------------------------------|
|          | This Study | Literature          |
| CS       | 38.54      | 34–43 [69,70]      |
| CLA      | 31.47      | 30–34 [71,72]      |
| PVDF     | 26.26      | 22–29 [73,74]      |

To evaluate the changes in the intermolecular interactions at the interface nanocomposites-water after incorporation of the TiO2 NPs, the interfacial tension $\gamma_{sl}$ was calculated using Equation (8) and summarized in Table 7. According to the observations on the surface energy, there was also an increase of the $\gamma_{sl}$ with filler rates for all nanocomposites. In particular, for the same rate of $\Phi$, we find that the $\gamma_{sl}$ was more important in the order PVDF/TiO$_2$-Water < CLA/TiO$_2$-Water < CS/TiO$_2$-Water.

Table 7. Interfacial tension of CS/TiO$_2$, CLA/TiO$_2$ and PVDF/TiO$_2$ with water as function $\Phi$ of TiO$_2$ NPs.

| $\Phi$ (%) (TiO$_2$) | $\gamma_{sl}$ $(10^{-3}$ J m$^{-2}$) |
|----------------------|----------------------------------|
|                      | CS/TiO$_2$ | CLA/TiO$_2$ | PVDF/TiO$_2$ |
| 0                    | 43.16      | 41.92      | 39.18        |
| 10                   | 45.23      | 43.04      | 40.32        |
| 20                   | 49.09      | 46.25      | 43.40        |
| 30                   | 54.43      | 51.20      | 48.22        |

Interestingly, during the incorporation of TiO2 NPs, the bio-based CS/TiO2 and CLA/TiO$_2$ nanocomposites exhibit an improved $\gamma_s$ as well as and $\gamma_{sl}$ than for PVDF/TiO$_2$ synthetic one.

3.2. Contact Angle and Capillary Pressure

As mentioned in Section 2.1.1, for nanopore with radius $r_p$ (1–10 nm) < $\lambda_c$ (water) = 2.7 mm, the effect gravitational force on the contact angle configuration is then neglected and only the intermolecular vdW surface forces contribute to the contact angle [36] (p. 36).

To study the capillary pressure behavior of the nanocomposites, we first determined the contact angle at the three-phase boundary between nanocomposite-water-air using Young’s relation (relation 7). Figure 3 shows a decrease of the contact angle for all nanocomposites with increasing the volume fraction of TiO2 NPs. The CS, CLA and PVDF polymer matrix ($\Phi = 0\%$) exhibits a hydrophobic behavior with the water contact angle > 90°. Simultaneously, we can see from Tables 5 and 7 for $\Phi = 0\%$, the interfacial tension $\gamma_{sl}$ is greater than surface energy $\gamma_s$ of polymer matrix which leads to the formation of a convex meniscus ($P_c = P_{nw} - P_w < 0$) at the interface water-air that prevent water to flow inside of the nanopore.

After incorporation of TiO2 NPs, a conversion from hydrophobic to hydrophilic character for CS/TiO$_2$ nanocomposite is identified at $\Phi < 10\%$, while the hydrophobic character persists by filling with 10% < $\Phi < 20\%$ for CLA/TiO$_2$ and PVDF/TiO$_2$ nanocomposites. Therefore, the CS/TiO$_2$ nanocomposite provides enhanced hydrophilic behavior with low filling with TiO2 NPs than CLA/TiO$_2$ and PVDF/TiO$_2$ nanocomposites.

For depicting the changes in the contact angle on the capillary pressure, we calculated the evolution of the capillary pressure as function of the nanopore radius (1–10 nm) using relation 2. Then, we normalized the capillary pressure $P_c$ to the atmospheric pressure ($Pa = 101.325$ kPa) to show the rate of changes caused by the incorporation of TiO$_2$ NPs.
were, respectively, 5.1%, 10.90%, and 13.90%. In Table 8, we summarized the corresponding values which reveals a changing from draining to filling of water inside the nanopores. However, as noted in Figure 4b, the normalized capillary pressure for CS/TiO2 nanocomposite is identified at Φ = 5.1% and the capillary pressure tends to pull water from unwetted to wetted regions of the nanopore (Figure 2a), resulting in the drainage of water from the nanopore. In the other hand, such negative capillary pressure describes the necessary opposite pressure to provide rising water inside the nanopore in the case of the use of a nanofilter based on a purely polymer matrix. Therefore, for the CS, CLA, and PVDF polymeric nanofilter membranes, the NF process requires supplementary pressure with opposite and higher strength than the capillary pressure to squeeze water throughout the nanopore.

For a pure polymer matrix (Figure 4a), the normalized capillary pressure was negative along the nanopore radius r_p. As can be interpreted from relation 2, the negative value of P_c originates hydrophobic behavior of the CS, CLA and PVDF polymer matrix which leads to negative value of the term cosθ (Figure 3). Consequently, the meniscus is convex, and the capillary pressure tends to pull water from unwetted to wetted regions of the nanopore (Figure 2a), resulting in the drainage of water from the nanopore. In the other hand, such negative capillary pressure describes the necessary opposite pressure to provide rising water inside the nanopore in the case of the use of a nanofilter based on a purely polymer matrix. Therefore, for the CS, CLA, and PVDF polymeric nanofilter membranes, the NF process requires supplementary pressure with opposite and higher strength than the capillary pressure to squeeze water throughout the nanopore.

We now turn to study the capillary pressure after incorporation of the TiO2 NPs. As noted Figure 4b, the normalized capillary pressure for CS/TiO2-10 becomes positive which reveals a changing from draining to filling of water inside the nanopores. However, for CLA/TiO2-10 and PVDF/TiO2-10, the normalized capillary pressure becomes less important than for CLA and PVDF purely matrix but it still drains water from the nanopores. However, as demonstrated in Figure 4c,d for Φ = (20%, 30%), the capillary pressure becomes positive for all nanocomposites and still increases with increasing the volume fractions of TiO2 NPs.

Figure 5 depicts the relative evolution of the capillary pressure for Φ = (20%, 30%) at the same effective nanopore radius r_pe = 5 nm. For all nanocomposites, the P_c/P_a (Φ = 30%) ≈ 2. P_c/P_a (Φ = 20%). Interestingly, this demonstrates that the capillary pressure increases almost twofold with the addition rate of 10% (from 20% to 30%) of TiO2 NPs. In addition, it should be noted that the capillary pressure was more important in the order PVDF/TiO2 < CLA/TiO2 < CS/TiO2 nanocomposites.

Therefore, for future experimental valorizations of these finding, it is crucial to determine the threshold volume fraction that corresponds to conversion from draining to filling by capillary pressure. To do so, we determined the threshold of the volume fraction Φ_th of TiO2 NPs for what the contact angle equal 89.9°. Correspondingly, Φ_th at which there is a transition from P_c < 0 that is in favor of draining, to P_c > 0 that is in favor of capillary filling. As depicted in Figure 4, the Φ_th for CS/TiO2, CLA/TiO2 and PVDF/TiO2 were, respectively, 5.1%, 10.90%, and 13.90%. In Table 6, we summarized the corresponding threshold dielectric constant ε_th, refractive n_th, Hamaker constant H, the surface energy γ_th for CS/TiO2, CLA/TiO2, and PVDF/TiO2 nanocomposites.
Figure 4. Capillary pressure as function of the pore radius for CS/TiO$_2$, CLA/TiO$_2$ and PVDF/TiO$_2$: (a) $\Phi = 0\%$, (b) $\Phi = 10\%$, (c) $\Phi = 20\%$, (d) $\Phi = 30\%$.

Figure 5. Normalized capillary pressure $P_c/P_a$ at $r_{pe} = 5$ nm and $\Phi = (20\%$ and $30\%)$ for CS/TiO$_2$, CLA/TiO$_2$ and PVDF/TiO$_2$ nanocomposites.
3.3. Capillary Rise

We highlighted the effect of TiO₂ NPs on surface energy, capillary pressure, and contact angle in the previous section. Now, we will explore the dynamics aspects of the filling of water by evaluation of capillary rise and volume uptake of water throughout the NF membrane for \( \phi > \phi_{\text{th}} \), i.e., when water flows inside the nanopore of the membrane under action of capillary pressure. Therefore, the capillary rise \( (y(t)) \) and water filling dynamics \( (V(t)) \) of water in nanocomposites were restrictively studied for CS/TiO₂ at \( \phi = (10\%, 20\% \) and 30\%) > \( \phi_{\text{th}} \) (CS/TiO₂) = 5.1\%, and for CLA/TiO₂ and PVDF/TiO₂ at \( \phi = (20\% \) and 30\%) > \( \phi_{\text{th}} \) (PVDF/TiO₂ > \( \phi_{\text{th}} \) (CLA/TiO₂). For comparative purposes, they will juxtaposed with those and the \( y_{\text{th}}(t) \) and \( V_{\text{th}}(t) \) threshold ones.

To demonstrate the negligible effect of gravity in capillary filling kinetics, we show the gravity and capillary forces for each nanocomposite with effective nanopore radius \( r_{pe} = 5 \text{ nm} \). As it can be observed in Figure 6a, the capillary force balance with gravity force only for \( y_t \) that is over \( y > 10 \text{ m} \) that is very higher to the ordinary dimension of the nanofilter. Incidentally, for \( y < 10 \text{ m} \), the gravity force was less than capillary force by one order of magnitude \( f_g < 10^{-1} f_c \) (Figure 6b), which is in good agreement with previous studies [19] (p. 1624), [36] (p. 47). Consequently, for the here examined rise levels restricted by the maximum nanofilter height to less than 1 m, the contribution of the gravity force on the capillary filling kinetic of the water inside the nanopores is neglected \( (f_g << f_c) \).

| Nanocomposite | CS/TiO₂ | CLA/TiO₂ | PVDF/TiO₂ |
|---------------|---------|----------|-----------|
| \( \phi_{\text{th}} \) (%) | 5.10 | 10.90 | 13.90 |
| \( n_{\text{th}} \) | 1.57 | 1.57 | 1.55 |
| \( \phi_{\text{th}} \) | 6.83 | 7.92 | 13.24 |
| \( H (10^{-20} \text{ J}) \) | 9.08 | 8.97 | 8.55 |
| \( \gamma_{\text{th}} (10^{-3} \text{ J m}^{-2}) \) | 43.83 | 42.62 | 41.51 |

Figure 6. Gravity and capillary forces as function of distance rise in one nanopore: (a) the gravity force balance capillary force for at \( y_t \), (b) the strength of gravity force is negligible compared to the capillary force for distance (1 nm to 9 m).

Therefore, the capillary rise is governed only by the balance between the viscous friction force \( (f_g) \) and capillary force \( (f_c) \). It is the so-called viscous regime, during which the capillary filling is well described by Washburn’s law (Section 2.1.2). Hereafter, to carry out the effect of the volume fraction on the capillary rise, we consider single capillary nanopore of uniform internal circular cross section with effective radius \( r_{pe} = 5 \text{ nm} \).
Figure 7 shows that the capillary rise \( y(t) \) increase with increasing volume fraction of TiO\(_2\) NPs. Obviously, the water rises spontaneously in nanopores under action of capillary pressure and without any other additional force for all nanocomposites. Interestingly, this result supports our idea for capillary-driven NF using nanoporous CS/TiO\(_2\), CLA/TiO\(_2\) and PVDF/TiO\(_2\) nanocomposites as nanofiltration process with zero energy consumption. Typically, the rise times in our study are in agreement with recent experimental and simulation studies [20,75]. In fact, for capillary nanopore, water rises slowly over time because the viscous friction forces become more important for nanoporous narrowed capillary, which reduces the overall capillary dynamics significantly.

![Figure 7](image_url)

**Figure 7.** Effect of the volume fraction of TiO\(_2\) NPs on capillary rise \( y(t) \) with \( r_{pe} = 5 \) nm: (a) CS/TiO\(_2\), (b) CLA/TiO\(_2\), (c) PVDF/TiO\(_2\), (d) \( y/y_{th} \) as function of \( \phi \) of TiO\(_2\) NPs.

In accordance with Section 3.2, for \( \phi = 10\% \), only the CS/TiO\(_2\)-10 nanocomposite that exhibits a capillary rise (Figure 7d). Contrarily, for the CLA/TiO\(_2\)-10 and PVDF/TiO\(_2\)-10, the capillary pressure remains negative, which prevents the rise of water inside the nanopores. However, for \( \phi = (20\% \text{ and } 30\%) \) (Figure 7a–c), all the nanocomposites exhibit spontaneous capillary rise. As expected from the study of capillary pressure, the capillary rise increases with volume fraction of the TiO\(_2\) NPs.

Figure 7d depicts the increases rates of the normalized capillary rise \( (y/y_{th}) \) with volume fraction filler of TiO\(_2\) NPs. In particular, at \( \phi = 30\% \), the \( y/y_{th} \) were about \( \sim 17 \), \( \sim 15 \) and \( \sim 14 \), respectively, for CS/TiO\(_2\), CLA/TiO\(_2\) and PVDF/TiO\(_2\) nanofilter. Interestingly, this finding demonstrates that the biodegradable CS/TiO\(_2\) and CLA/TiO\(_2\) nanofilter exhibit higher capillary rise than the synthetic PVDF/TiO\(_2\) nanofilter. From a review of Tables 3 and 5, we can thus reveal that the enhancement of the capillary rise can be made by increasing the refractive index of the based nanofilter materials.
3.4. Effect of Volume Fraction of TiO$_2$ NPs on Capillary-Driven Water Volume

As detailed in Section 2.1.3, the modified LW model allows the calculation of the capillary-driven water volume throughout nanoporous membrane as a function of the morphological characteristics of the nanofilter, ($\phi$, $r_{pe}$, $\delta$ and $\tau$), the physical properties of the water, ($\rho$, $\eta$, and $\gamma_l$), and the contact angle $\theta$ which depends on the volume fraction of TiO$_2$ NPs.

Therefore, to explore the effect of the incorporation of TiO$_2$ NPs on the capillary-driven water volume, we consider that the morphological characteristics the nanocomposite nanofilter are the same for all nanocomposites. Hereafter, we consider the porosity of nanofilter $\phi = 0.7$ with corresponding tortuosity $\tau = 1.27$ (Relation 6) and non-circular cross section of nanopores with roundness $\delta = 0.5$.

The capillary-driven water volume was calculated for surface nanofilter membrane $S = 1$ m$^2$ and effective nanopore radius $r_{pe} = 5$ nm using relation 5. As shown in Figure 8a–c, for $\phi = \phi_{th}$ (CS/TiO$_2$-5.1 $\cong$ CLA/TiO$_2$-10.9 $\cong$ PVDF/TiO$_2$-13.9), the threshold capillary-driven water volume ($V_{th}$) after one hour of filling was $\sim 30$ mL. In fact, at $\theta_{th} = 89.9^\circ$, the term $\cos(\theta_{th})$ in Equation (5) is equal $1.7 \times 10^{-3}$, which leads to a weak value of $V_{th}$.

However, for $\phi = 10\%$ (Figure 8a–d), only the CS/TiO$_2$-10 nanocomposites’ nanofilter exhibits a spontaneous capillary-driven nanofiltration with $V \approx 3$ L·h$^{-1}$. In agreement
with capillary pressure (Section 3.2) and capillary rise (Section 3.3), this finding indicates the enhanced capillary-driven NF of CS/TiO$_2$-10 nanocomposite in comparison with other CLA/TiO$_2$-10 and PVDF/TiO$_2$-10 nanocomposites, which do not demonstrate a capillary-driven flow at $\phi = 10\%$.

While, for $\phi = (20\%$ and $30\%)$, we clearly observe in Figure 8b-c-d a great increase of the capillary-driven water volume. In particular, CS/TiO$_2$-30 has the highest capillary-driven nanofiltration with $V = 6.39$ L·h$^{-1}$, followed by CLA/TiO$_2$-30 with $V = 5.76$ L·h$^{-1}$ and PVDF/TiO$_2$-30 with $V = 5.26$ L·h$^{-1}$. Accordingly, it is important to note that these orders of magnitude of capillary-driven water volume are directly in line with previous findings ($2-25$ L·h$^{-1}$·m$^{-2}$) [17,40,76]. This validates our theoretical findings on the one hand, and motivate future experimental valorizations of this study on the other.

Interestingly, for the same incorporation rates $\phi = (20\%$ or $30\%)$ of the TiO$_2$ NPs, the increased $V(t)$ of the CS/TiO$_2$, in comparison to CLA/TiO$_2$ and PVDF/TiO$_2$ nanocomposites nanofilter, originate from the elevated surface energy of the CS polymer matrix ($\gamma_s (CS) = 38.54$ J·m$^{-2}$) > ($\gamma_s (CLA) = 31.47$ J·m$^{-2}$) > ($\gamma_s (PVDF) = 26.26$ J·m$^{-2}$), which strongly proportional to the refractive index of the polymers matrixes ($n (CS) = 1.53$) > ($n (CLA) = 1.47$) > ($n (PVDF) = 1.42$). In addition, from study of the capillary-driven water volume, we demonstrate that all nanocomposites are prominent candidates for use as domestic supplementary purification of drinking water for removal of microparticle waste with zero energy consumption.

Crucially, the biodegradable CS/TiO$_2$-30 and CLA/TiO$_2$-30 nanocomposites nanofilter demonstrate capillary-driven water volume higher ~1.5 and ~1.2 times, respectively, more than the synthetic PVDF/TiO$_2$-30 nanocomposite. In particular, CS/TiO$_2$ nanocomposite offer the most improved capillary-driven NF behavior during the incorporation of the TiO$_2$ NPs.

It is important to note that for the experimental validation, the nanocomposite materials do not have the same morphological characteristics (tortuosity, porosity, pore size, etc.). Therefore, the capillary-driven water volume calculated by the modified L-W model (relations 5 and 6) is directly proportional to the pore radius, shape factor, porosity, and cross section nanofilter, and inversely proportional to the tortuosity of the nanofilter materials.

The methodologies used along this study constitute simple and complete theoretical methods for prediction the wettability as well as the spontaneous capillary pressure and the capillary-driven flow for any material with known refractive index dielectric permittivity and physical properties of the fluids.

Overall, these findings constitute a quantitative and qualitative background for further experimental elaboration of capillary-driven nanofilter based on green and biodegradable CS/TiO$_2$ and CLA/TiO$_2$ nanocomposites.

4. Conclusions

In this study, from Lifshitz and Young-Laplace theories, it is shown that the polymer matrixes CS, CLA and PVDF provide hydrophobic contact angle ($\theta > 90^\circ$) and draining capillary pressure. Consequently, the pure polymers matrix does not perform a capillary-driven flow and then cannot be used as capillary-driven nanofilter for water purification.

However, after incorporation of TiO$_2$ NPs, a wetting conversion from hydrophobic to hydrophilic were depicted for all CS/TiO$_2$, CLA/TiO$_2$ and PVDF/TiO$_2$ with, respectively, threshold volume fraction TiO$_2$ NPs for wetting conversion equal to 5.1%, 10.9%, and 13.9%.

For incorporation with $\phi > \phi_{th}$, the contribution of gravity forces on capillary rise as well as the capillary-driven flow is neglected for the considered nanofilter with effective nanopore radius $r_{pe}$ (~10 nm) < $\lambda_c$ (water) =2.7 mm and with macroscopic size of nanofilter < 10 m.

For a single nanopore, an increase of capillary rise with increased volume fraction was demonstrated for all CS/TiO$_2$, CLA/TiO$_2$ and PVDF/TiO$_2$ nanocomposites. However, for the same incorporation rates of TiO$_2$, the biodegradable CS/TiO$_2$ and CLA/TiO$_2$ exhibits a higher capillary rise than PVDF/TiO$_2$. This increase was attributed to the higher surface...
energy proportional to the refractive index of the dielectric permittivity. Consequently, this fact revealed that water rise in nanopores without the help of any external force for all nanoporous nanocomposites. This important finding supported our proposed idea for capillary-driven nanofiltration as zero energy consumption nanofiltration process.

Based on the modified L-W model, we demonstrated that capillary-driven water volume for CS/TiO$_2$, CLA/TiO$_2$, and PVDF/TiO$_2$ nanocomposites increases with increasing TiO$_2$ NPs volume fraction. Interestingly, at 30% volume fraction of TiO$_2$ NPs, the biodegradable CS/TiO$_2$ and CLA/TiO$_2$ nanocomposites nanofilter demonstrate capillary-driven water volume higher by ~1.5 and ~1.2 times, respectively; more than the synthetic PVDF/TiO$_2$ nanocomposite.

Collectively, CS/TiO$_2$ and CLA/TiO$_2$ biodegradable nanocomposites were the better candidates for purification of drinking water by capillary-driven nanofiltration process as sustainable, environmentally safe, and zero energy consumption.

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