Influence of stoichiometry on indentation-induced plasticity in CuZr glasses

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Abstract
Plasticity in metallic glasses depends on their stoichiometry. We explore this dependence by molecular dynamics simulations for the case of CuZr alloys using the compositions Cu$_{64.5}$Zr$_{35.5}$, Cu$_{50}$Zr$_{50}$, and Cu$_{35.5}$Zr$_{64.5}$. Plasticity is induced by nanoindentation and orthogonal cutting. Only the Cu$_{64.5}$Zr$_{35.5}$ sample shows the formation of localized strain in the form of shear bands, while plasticity is more homogeneous for the other samples. This feature concurs with the high fraction of full icosahedral short-range order found for Cu$_{64.5}$Zr$_{35.5}$. In all samples, the atomic density is reduced in the plastic zone; this reduction is accompanied by a decrease of the average atom coordination, with the possible exception of Cu$_{35.5}$Zr$_{64.5}$, where coordination fluctuations are high. The strongest density reduction occurs in Cu$_{64.5}$Zr$_{35.5}$, where it is connected with the partial destruction of full icosahedral short-range order. The difference in plasticity mechanism influences the shape of the pileup and of the chip generated by nanoindentation and cutting, respectively.

Keywords Metallic glass · Plasticity · Indentation · Shear bands · Molecular dynamics

1 Introduction

The mechanical properties of metallic glasses (MGs) are sensitive to the processing history [1, 2] and also to their atomic composition. This is due to the formation of short-range order (SRO) motifs that are strictly linked to the preparation method [3–5] and to the stoichiometry [4, 6–8]. As most relevant motif, the so-called full icosahedral (FI) clusters centered on Cu atoms have been identified [3]. The presence of this type of polyhedra effectively reduces the free volume between the atoms and thus has been related to the formation of more stable MGs, i.e., more relaxed samples [5, 7–11].

The effects of variation in atomic composition have been studied in the CuZr MGs, and it has been shown that a composition with around 75% Cu content forms the maximum number of FIs [7, 8]. Increasing the Cu content results in a higher Young’s modulus and yield strength [8]. However, in such compositions, the plastic flow is reduced by the rapid formation and propagation of shear bands [12–15]. Thus, compositions with Cu content > 50% are preferred to study the shear-band phenomenon in MGs [16–19].

In the present work, we study the plasticity in three compositions of CuZr MG, namely Cu$_{64.5}$Zr$_{35.5}$, Cu$_{50}$Zr$_{50}$, and Cu$_{35.5}$Zr$_{64.5}$. Plasticity in the MGs is induced by simulated indentation. However, we show in the Appendix 1 that comparable results are obtained for another way of inducing plastic flow in the MGs, namely by orthogonal cutting of the samples. We analyse the local changes occurring in the polyhedral clusters present after machining the samples and
find that most of the deformation occurs via the annihilation of the FIs for the samples containing a high fraction of Cu. In the case of the sample with the smallest Cu concentration, the creation of polyhedra with coordination numbers 12 and 13 is observed.

2 Simulation details

Three different CuZr MG compositions were created by using the open-source code LAMMPS [20], namely Cu$_{64.5}$Zr$_{35.5}$, Cu$_{50}$Zr$_{50}$, and Cu$_{35.5}$Zr$_{64.5}$. The interaction between the atoms is modeled via an embedded-atom-method potential [21]. The samples have approximate dimensions of 56 nm × 22 nm × 45 nm in the x, y, and z directions, respectively (see Fig. 1), containing more than $3 \cdot 10^6$ atoms. For the preparation of the samples, a crystalline mixture of the appropriate stoichiometry is first heated to a temperature $T = 2000$ K for a time period of 500 ps. Then, the molten mixture is cooled down to a final temperature of $T = 0.1$ K at a rate of 0.01 K/ps. The cooling is performed under periodic boundary conditions using an isobaric ensemble with a Nose-Hoover thermostat. After cooling, the sample is relaxed with periodic boundary conditions for 200 ps. Subsequently, the boundary condition in the top surface is changed to a free boundary, and the samples are relaxed for an additional time of 300 ps before indentation.

During indentation, a layer of 2.8-nm-width is fixed at the bottom of the samples to avoid any center-of-mass translation. Also, the temperature is kept fixed by using an NVT ensemble. The indenter has a cylindrical shape with a radius of $R = 7$ nm; it is modeled by a repulsive potential [22] with a stiffness constant of 10 eV/Å$^3$. Initially, the indenter is positioned just above the sample surface and then is moved in the $-z$ direction at a velocity of 20 m/s to a total indentation depth of 7 nm.

We use the open-source visualization tool (OVITO) [23] to calculate the atomic shear strain and to determined the polyhedral clusters characterizing the SRO in the samples.

3 Results

3.1 Polyhedral clusters in the undeformed samples

Before applying a deformation, we analyse which polyhedral clusters are present in our three different compositions, shown in Fig. 2. Polyhedral clusters are conveniently analyzed by the number of polygonal faces of the Voronoi polyhedron around the central atom; thus, icosahedral clusters are denoted as $(0, 0, 12, 0)$, indicating that 0 triangular, quadrangular, or hexagonal faces are present besides the 12 pentagons defining the icosahedron. Fig. 2 provides the averages over Cu-centered and Zr-centered polyhedra in the samples. The figure shows that for the case of Cu$_{64.5}$Zr$_{35.5}$, the FI clusters are the predominant type of the SRO motifs with a fraction of 16%. In comparison, the percentage of FI clusters is significantly smaller in the compositions Cu$_{50}$Zr$_{50}$ and Cu$_{35.5}$Zr$_{64.5}$ with a fraction of 6% and 2%, respectively. This is consistent with experiments [8] and previous simulations [7] where the maximum of pentagonal polyhedra was found for a Cu concentration of 75%. Nonetheless, here these clusters are still the dominant type for the composition Cu$_{50}$Zr$_{50}$. In the case of the

![Fig. 1 Schematic setup of the nanoindentation simulations.](image1)

![Fig. 2 List of the most frequent Voronoi polyhedra found in the three compositions. The coordination number (CN) of the central atom in the cluster is indicated.](image2)
composition Cu$_{35.5}$Zr$_{64.5}$, the most dominant clusters are the $(0, 2, 8, 4)$ and $(0, 2, 8, 2)$ polyhedra.

It is well known that local icosahedral ordering reduces both the local atomic volume and the potential energy of the central atom below that in an hcp or fcc environment [24]. Hence full icosahedral clusters $(0, 0, 12, 0)$ of icosahedra are Cu-centered, since the atomic volume of Cu is smaller than that of Zr. As Ma [10] argues, small perturbations of the fully icosahedral structure can change the local order to $(0, 2, 8, 2)$ or $(0, 3, 6, 3)$; both motifs are amply found in Fig. 2.

Even for the Cu-poor sample, Cu$_{35.5}$Zr$_{64.5}$, the number of pentagons in the nearest-neighbor shell is always dominant, Fig. 2, giving evidence of the non-periodic constitution of this material. Zr, being the larger of the two elements, prefers a higher local coordination (CN=16 [10]), changing the local polyhedral motifs. As Cheng and Ma [25] point out, the number of Zr-centered motifs increases with Zr content, but no dominant motif, replacing the Cu-centered FIs, can be identified.

### 3.2 Shear bands and pileup

After indentation, the deformation created in the samples with 50% and 35.5% Cu concentration forms a different pattern than the one with 64.5% Cu. This can be observed in the von-Mises shear strain (VMSS) maps shown in Fig. 3. This figure compares the composition Cu$_{64.5}$Zr$_{35.5}$ (a-c) and Cu$_{50}$Zr$_{50}$ (d-f) at indentation depths $d = 5$ nm (a and d), 6 nm (b and e), and 7 nm (c and f). For the Cu$_{64.5}$Zr$_{35.5}$ composition, plasticity is strongly localized, i.e., it is characterized by the formation of shear bands. These already show up at intermediate indentation depths, $d = 5$ nm, but intensify with deeper indentation. In the case of Cu$_{50}$Zr$_{50}$, the deformation is homogeneous and consists mostly of unorganized local shear regions called shear transformation zones (STZs). We do not show the results for the sample Cu$_{35.5}$Zr$_{64.5}$ as they are very similar to Cu$_{50}$Zr$_{50}$. This behavior is not unique to indentation; we show in the Appendix 1 that cutting the same samples results in better defined shear bands for the composition with maximum Cu content.

Moreover, it can be observed in Fig. 3 that the shape of the pileup is different for the two different compositions. For the Cu$_{64.5}$Zr$_{35.5}$ composition, the pileup formed features abrupt changes of the slope; these are generated when shear bands intersect the surface. In addition, the pileup features a left-right asymmetry. This asymmetry is due to the shear band that formed at the left side of the sample, which was initiated around the indenter and exited the sample at the bottom of the pileup. In contrast, the composition Cu$_{50}$Zr$_{50}$ formed a symmetric and broader pileup with a continuously changing slope.

### 3.3 Shear strain, coordination, and polyhedral clusters in the deformed samples

We analyse the deformation in more detail by measuring quantitative changes in the samples with respect to the distance from the indenter surface. In order to perform this analysis, we divide our sample into several cylindrical shells, starting at the indenter surface and then continuing toward the sample interior. For each cylindrical shell, we measure the averaged VMSS, the FI fraction, and the total number of atoms within the shell divided by the volume of the shell, i.e., the atomic density $\rho$. The cylindrical shells are separated by a radial distance of 2.77 Å, and their distance from the indenter surface is denoted as $r_p$. For this analysis, the pileup is not included. Also the region immediately adjacent to the indenter, $r_p \leq 0.831$ nm, is excluded, since here the
high indentation-induced compaction leads to dramatic density increases which destroys the icosahedral clusters almost entirely. The results of our analysis are displayed in Fig. 4.

It shows that the higher the Cu concentration, the higher the initial percentage of FI clusters, and the higher the atomic density. This has also been demonstrated in Refs. [7, 8], where the most compact structure of the glass is found around the stoichiometry where the concentration of icosahedra takes its maximum, i.e., at 75% Cu.

Furthermore, Fig. 4 shows that, as expected by the observations from Fig. 3, the VMSS takes its highest values around the indentation site and decays rapidly up to a distance $\sim$10 nm. While the decline of the VMSS with distance is similar in all samples, the sample with 64.5% Cu experiences a slightly higher shear strain close to the indenter surface. For this composition, for a radial distance $r_a < 5$ nm, around 8.2% of the FI clusters were destroyed by the indentation process. The FI clusters only reach their undeformed value $\sim$10 nm away from the indenter surface, corresponding to the point where the VMSS reaches a value close to zero. At the same time, a decrease in the atomic density can be observed at similar radial distances, with a minimum located closer to the indenter. In cutting simulations (see Appendix 1), a similar decrease in the FI clusters, and the density has been observed along the path of propagation of the shear bands. For indentation, however, the decrease in density around the indenter is rather surprising due to the type of deformation. Intuitively, an increase in the atomic density would be expected since the pressure exerted by the indenter leads to an atomic compression. Having the opposite effect indicates that the decrease in the density due to the breakage of the most compact clusters is more significant than the increase in the density created by the compression of the indenter. Additionally, the formation of the pileup creates an additional path for material to move upward, thus releasing the stress created by the indenter.

The Cu$_{50}$Zr$_{50}$ sample shows a similar behavior as the one seen for Cu$_{64.5}$Zr$_{35.5}$ in Fig. 4. However, for the former, the effects of the deformation on the FI clusters are considerable smaller, accounting for a maximum decrease of only 1.8% reached at a distance of $\sim$6.6 nm away from the indenter surface. Surprisingly, for the sample with the smallest Cu content, the opposite effect can be observed, where we observe an increase of $\sim$1% of the FI clusters around the indentation site, albeit starting from a very small level (1.7%). The increase in the tightly coordinated FIs explains why the density decrease in this sample is relatively moderate.

Before deformation, the average coordination in the samples increases with Zr content, see Fig. 5, since Zr has a larger atomic radius than Cu. This figure also shows how the average atomic coordination changes in the vicinity of the indenter as a function of the distance to the indenter surface, $r_a$. While for Cu$_{35.5}$Zr$_{64.5}$, the changes seem to be unsystematic, for Cu$_{50}$Zr$_{50}$ and in particular Cu$_{64.5}$Zr$_{35.5}$ a...
clear decrease of the average coordination in the plastic zone can be observed.

We shall study this effect in more detail and also investigate the effects of the deformation on the initial motifs. For this analysis, we do not consider the list of polyhedra as detailed in Fig. 2. Rather, we mix all polyhedra with the same coordination number (CN) and measure the local variations with respect to the distance to indenter surface, $r_a$.

Fig. 6 shows the results of this analysis. Note that the FI clusters, $(0, 0, 12, 0)$, have CN=12. In this figure, as in Fig. 5 above, we increased the width of the radial shells to 2.7 nm to better average over small fluctuations. In order to study the changes that take place at the location where the maximum deformation occurs, one can use the VMSS data from Fig. 4. Thus, the main observations that can be extracted from Fig. 6 are as follows.

- The motifs with coordination number CN≥15 decreased after the deformation in the three compositions.
- For Cu$_{64.5}$Zr$_{35.5}$, the annihilation of the preferred motifs close to the indentation site is more dramatic than the creation of new ones, with the deformation being mostly governed by the breakage of the motifs with CN=12. These clusters are mainly constituted by the FIs according to Fig. 4.
- For the Cu$_{50}$Zr$_{50}$ sample, the total number of polyhedral annihilation decreased in comparison to the Cu$_{64.5}$Zr$_{35.5}$ sample. Also, the creation of the motifs with CN=13 increases to around 1% in comparison to the Cu$_{64.5}$Zr$_{35.5}$ sample.
- A decrease of density caused by the plastic deformation is observed in all glasses. Such a density decrease corresponds to experimental [26] and previous simulational [27, 28] observations. The plastic motion of atoms introduces defects into the material which lower the local density; this effect is most pronounced in the best-ordered structures, i.e., in the Cu-rich samples with their frequent icosahedral motifs.
- In the Cu$_{35.5}$Zr$_{64.5}$ sample, the population of the clusters with CN=12 increases to above 1.5%. This is different to the observations in the other two samples. Also, there is an increase of motifs with CN=13 to 1.5% in comparison to the undeformed sample. Overall, for this composition, the creation of new clusters is faster than their annihilation.
- The deformation of the Cu$_{35.5}$Zr$_{64.5}$ sample seems to have a longer-ranged effect, as can be seen in the data for the cluster with CN=13. In this particular case, even at a distance of $r_a = 20$ nm, a change of ~0.5% can be still observed, while for the other samples, at this distance, the pre-deformation values are reached.

Interestingly, the results described above are similar to results obtained in a cutting simulation (see Appendix 1). In any particular composition, the motifs affected in the region of maximum shear are the same in the indentation simulation and in the cutting simulation. Moreover, the percentage change is also similar in both types of simulations. This suggests that the results depend on the sample structure—in particular the initial FI content, which depends on sample preparation and relaxation as well as on stoichiometry—rather than the deformation dynamics.

We conclude that plastic deformation in all glasses leads to a decrease of density. This decrease is most pronounced (up to 4 %) for high Cu content and is accompanied by the destruction of FIs and other highly coordinated clusters. The case of small Cu content, Cu$_{35.5}$Zr$_{64.5}$, shows an increase in FIs and also of other 12- and 13-fold coordinated clusters, while clusters with CN ≥ 14 are destroyed, and the density decrease is mild (2 %).
3.4 Plastic zone

In this section, we analyse the plastic zone created by the indenter for the three different compositions.

In order to analyse the structure of the plastic zone further, we define as ‘plastically active atoms’ those that suffer a von-Mises shear strain above a certain threshold, which we choose here as VMSS > 0.3 [29]. The spatial structure of these plastic zones is depicted in Fig. 7. The plastic zone appears to be more homogeneously distributed around the indenter for Cu_{50}Zr_{50} and Cu_{35.5}Zr_{64.5} than for Cu_{35.5}Zr_{64.5}. The inhomogeneous structure of the plastic zone is caused by the shear bands that extend out into the sample.

We determine the density of these plastically active atoms, \( \rho_a \), as a function of the distance from the indenter surface, \( r_a \), in a similar way to the quantities obtained in Fig. 4, see Sect. 3.3. The results are shown in Fig. 8 where, as discussed above, the data of the two cylindrical shells closest to the indenter surface are omitted. The dashed lines in Fig. 8 correspond to the densities of the undeformed system for comparison. It can be observed that close to the indenter there is a plateau in the density close to the value of the undeformed system. This means that close to the indenter almost all the atoms participate in the deformation. The density values at the plateau differ farther from the undeformed values as the Cu concentration increases. This is consistent with the results found in Fig. 8, where it was shown that the atomic density decreases further with higher Cu concentration. The plateau extends farther out for smaller Cu concentration indicating a bigger core of the plastic zone. This finding coincides with Fig. 7, where the plastic zone appears to be more homogeneously distributed around the indenter for Cu_{50}Zr_{50} and Cu_{35.5}Zr_{64.5}. The density of the plastic zone decays similarly for the cases Cu_{50}Zr_{50} and Cu_{35.5}Zr_{64.5}, indicating that despite the difference in the initial atomic density, the final extensions of the plastic zones are almost identical.

In the case of Cu_{64.5}Zr_{35.5}, the density of plastically active atoms decreases faster than in the other cases. However, after \( \sim 7.5 \) nm, the behavior changes and the density of Cu_{64.5}Zr_{35.5}

decreases more slowly than for the other two samples; this behavior is caused by the shear bands that extend out into the sample as seen in Fig. 7.

4 Summary

We performed molecular dynamics simulations of nanoindentation and orthogonal cutting of three samples of CuZr MGs to identify the differences in plasticity. Before deformation, the different compositions of the three samples showed up in a different content of SRO motifs, as was known already previously [7, 8, 10, 25]: whereas the sample with the highest Cu content, Cu_{64.5}Zr_{35.5}, is characterized by a high fraction of Cu-centered FIs, the contribution of FIs shrinks with decreasing Cu content, while no other structural motif takes a dominating role. The average coordination number of the three samples decreases with Cu content. Both nanoindentation and orthogonal cutting lead to comparable effects in the MG plasticity. Only for the highest Cu content, Cu_{64.5}Zr_{35.5}, plasticity is localized in shear bands, while in the glasses with lower Cu content, Cu_{50}Zr_{50} and
Cu_{35.5}Zr_{64.5}. STZs are generated in a homogeneous way without leading to shear localization. This feature is in agreement with the well-known mechanical superiority of Cu-rich CuZr glasses [8, 25].

In the plastic zone, the atomic density decreases. The strongest density reduction occurs in Cu_{64.5}Zr_{35.5}, where it is connected with the partial destruction of FI short-range order. With decreasing Cu content, the density reduction becomes less pronounced. The generation of free specific order. With decreasing Cu content, the density reduction is connected with the partial destruction of FI short-range order. All these features agree with previous findings discussed in Refs. [27, 32–34].

Moreover, the intensity of the colors of Fig. 10a–c suggests that the shear bands formed in the chip of the Cu_{64.5}Zr_{35.5} sample are better defined than in the other two compositions. This is confirmed by quantifying the VMSS in the chip as shown in Fig. 10d–e. It can be observed that for Cu_{64.5}Zr_{35.5}, Fig. 10d, the peaks in the VMSS—which indicate the position of the shear bands—are better distinguishable than in the other two cases (Fig. 10e and f).

The analysis shown in this figure was performed by slicing the chip in layers parallel to the PSZ with a thickness of 2.77 Å. Fig. 10d–f shows the data of the averaged VMSS per layer, the FI content and the density, \( \rho \), as a function of the distance from the PSZ, \( d_{PSZ} \), see Fig. 9. Here, the density \( \rho \) is calculated as the number of atoms in the layer divided by its length; it represents a layer density rather than the volumetric density that was shown in Fig. 2.

The changes in \( \rho \) and FI fraction in Fig. 10d–f show similar trends as in Fig. 2. \( \rho \) decreases where the shear strain increases, i.e., in the shear bands. Most interestingly, as in the case of indentation, the FI cluster fraction decreases where the deformation takes place for Cu_{64.5}Zr_{35.5} and Cu_{50}Zr_{50}, while it increases for the Cu_{35.5}Zr_{64.5}.

Finally, we analyse the changes in the motifs according to their coordination number in the chip as a function of the distance from the PSZ, \( d_{PSZ} \), in Fig. 11. To generate this figure, we increased the layer width to 2.7 nm, similar to the procedure to create Fig. 6. While this does not allow us to study the effects in the individual shear bands formed – since these are too narrowly spaced – we observe very similar results to the ones found in Fig. 6. For both types of deformation, the same motifs are being affected in the shear zones, as was discussed in detail in Sect. 3.3. This is the case for all the three samples.

We conclude that the changes in the plasticity with the composition of the MG found for indentation-induced plasticity hold equally for plasticity induced by a cutting process.

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Fig. 10 Top row: Side view of the compositions a Cu$_{64.5}$Zr$_{35.5}$, b Cu$_{50}$Zr$_{50}$, and c Cu$_{35.5}$Zr$_{64.5}$ for the cutting simulation at cutting length $l = 20$ nm. Atoms are colored according to their von-Mises shear strain (VMSS). Bottom row: d–f Dependence of the VMSS (black), full icosahedra (FI) clusters percentage (blue), and density (red), $\rho_f$, as a function of the distance to the PSZ, $d_{PSZ}$. The horizontal dashed lines give the values of the undeformed system.

Fig. 11 Cutting simulation: Percentage change of the coordination number (CN) as a function of the distance from the primary shear zone, $d_{PSZ}$, for a Cu$_{64.5}$Zr$_{35.5}$, b Cu$_{50}$Zr$_{50}$, and c Cu$_{35.5}$Zr$_{64.5}$. Data are for a cutting length of $l = 20$ nm.

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