Scattering of seismic waves can reveal subsurface structures but usually in a piecemeal way focused on specific target areas. We used a manifold learning algorithm called “the Sequencer” to simultaneously analyze thousands of seismograms of waves diffracting along the core-mantle boundary and obtain a panoptic view of scattering across the Pacific region. In nearly half of the diffracting waveforms, we detected seismic waves scattered by three-dimensional structures near the core-mantle boundary. The prevalence of these scattered arrivals shows that the region hosts pervasive lateral heterogeneity. Our analysis revealed loud signals due to a plume root beneath Hawaii and a previously unrecognized ultralow-velocity zone beneath the Marquesas Islands. These observations illustrate how approaches flexible enough to detect robust patterns with little to no user supervision can reveal distinctive insights into the deep Earth.

Therefore, previous approaches have limited utility in poorly sampled regions and do not make use of the full statistical power of waveform datasets that span geographically diverse paths.

We conducted a large-scale, systematic search for seismic waves scattered by heterogeneity near the CMB across the Pacific basin. We focused on shear waves diffracting along the CMB (Sdiff), because they sample large areas at the base of the mantle. Waves scattered by heterogeneity in this region arrive after the main Sdiff phase, so the timing and amplitude of these Sdiff “postcursors” can constrain the location and nature of structures producing the scattering (4, 6–9). Because energy reflected from the surface can complicate the identification of Sdiff postcursors, we restricted our attention to waveforms from deep earthquakes (10). This yielded a dataset of ~6000 transverse-component waveforms aligned on the main Sdiff arrival and deconvolved by synthetics computed for a one-dimensional (1D) preliminary reference Earth model (PREM) (11). When plotted by distance between the source and the receiver (Fig. 1A), postcursors cannot readily be identified. Ordering by azimuth only makes sense locally and is not useful when working with data spanning large geographic areas.

We made use of an unsupervised graph-based manifold learning algorithm, “the Sequencer” (10), that orders objects to minimize dissimilarities between neighbors as well as globally across the entire sequence. In our case, the objects are Sdiff waveforms and dissimilarity is given by the Wasserstein metric (also known as the earth mover’s distance) between them (10). This approach can be used to reveal the main trend present in a dataset without requiring any model at all; it has been used in astronomy and has already led to the discovery of a trend relating the mass of supermassive black holes to the properties of their host galaxies (12). We used the Sequencer to optimally order our collection of Sdiff waveforms across the Pacific basin (Fig. 1B). We identified postcursors in ~40% of waveforms, which indicates that postcursors are far more common than previously thought. Radial gradients in velocities cannot on their own explain the postcursors, regardless of ordering (Figs. S1, B and D, and S2).

We then explored the geographic distribution of heterogeneities giving rise to the postcursors by binning the fraction of waveforms with postcursors in 1° radius bins (Fig. 1C). We found that heterogeneities large enough to scatter shear waves with periods >15 s are pervasive across the Pacific basin. In most locations, a substantial fraction (~0.3) of waves show postcursors (Fig. 1C, cyan). Postcursors are typically absent (Fig. 1C, peach) on paths that do not cross LLSVP boundaries and instead are confined either within the boundaries or well outside of them. Waveforms with and without postcursors seem to coexist at subwavelength scales (~160 km) in most locations (Fig. 1C). Many of the postcursors in the western and northern Pacific (Fig. 1D, R2 and R3) have large delay times (fig. S3B), indicating that they originate from distant scatterers and may travel through complex structures. These areas are suspected to host a partial melt created by paleo-slab from northwestern Pacific subduction zones (13) and a group of small ULVZ patches, along with slab debris beneath the northeastern boundary of the mid-Pacific LLSVP (14). Although large-amplitude postcursors appear to be associated with a few localities south of the Aleutians (Fig. 1D, R3), bootstrap error estimates show that these signals are not statistically significant (fig. S4).

Notably, nearly all Sdiff wave sampling near Hawaii and the Marquesas Islands shows postcursors (Fig. 1C, pink). The amplitude of postcursors (with respect to the main Sdiff) in the Hawaiian region (Fig. 1D, R1) appears to be three times larger than the typical amplitude found throughout the Pacific basin (Fig. 1D, R2, R3, and R4).

When contextualized across all available data using the Sequencer, the region to the northwest of Hawaii stands out in terms of the prevalence of postcursors, their amplitude, and the spatial extent of the area associated with high-amplitude postcursors (Fig. 1, C and D). Therefore, we zoomed in on this region and performed a similar analysis of waveforms with turning points within 20° of Hawaii (Fig. 2A). The nature of such high-amplitude signals is discussed in the methods and materials section of the supplementary materials (10). By plotting the waveforms in the optimal order determined by the Sequencer, we readily identified a subpopulation featuring strong postcursors (Fig. 2B). Because of the limited geographic area, this population can...
also be identified by sorting the waveforms according to azimuth, with delay times increasing up to 40 s (fig. S5A). However, when visualized in the order determined by the Sequencer, the moveout of the postcursors is clarified, and coherent geographic patterns can be mapped.

By plotting each waveform’s position in the sequence at the midpoint of its diffracting path, we found that waveforms with postcursors appear to the northwest of Hawaii, whereas those without appear predominantly to the southeast (Fig. 1D, R4). Moreover, the order identified by the Sequencer reveals a very distinctive spatial pattern (Fig. 2E), with waveforms appearing late in the sequence flanking a region in which midsequence waveforms cluster. This coherent pattern is reflected in both delay time and amplitude of the post-cursors observed northwest of Hawaii (Fig. 2, C to E) and does not follow a simple azimuthal trend. Post-cursor delay times gradually increase toward the center of the cluster, whereas large-amplitude post-cursors (above ~0.5 with respect to the main Sdiff phase) are found mostly southward, near the northern edge of Pacific LLSVPs (Fig. 2E). The small number of weak post-cursors detected to the southeast (Fig. 1D, R4) does not show coherent geographic trends, suggesting that they were not produced by a structure of the type located beneath Hawaii.

We also observed an anticorrelation between post-cursor delay time and amplitude in the region (Fig. 2, C and D), consistent with expectations for a localized wave-speed anomaly. This observation motivated us to use the presence of such a correlation as a detector of localized structures. Thus, at each location across the Pacific basin, we estimated the slope and amplitude of the linear fit to the delay time and log amplitude of post-cursors with diffracting paths located within 5° of the location. As expected, we found steep negative slopes in the vicinity of Hawaii, across a region that is substantially larger than anywhere else in the Pacific basin (Fig. 3A). In addition, we also detected a similar signature, with a slightly gentler slope, close to the Marquesas (Fig. 3A), indicating a previously unidentified localized wave-speed anomaly. Near both hot spots, the negative slopes are significant at a 99% level of confidence (Fig. 3B). Other locations with possible detections of localized wave-speed anomalies are in the vicinity of Alaska, Kamchatka, and along the northern edge of the Pacific LLSVP, but none are as clear as those near the Marquesas.

After using the Sequencer to reveal the leading trend in our waveform dataset and map the presence of heterogeneity in the Pacific region, we investigated the physical origin of the post-cursor signals through waveform modeling. We carried out a systematic suite of wave-propagation simulations through candidate structures based on known features of the CMB region (16). Seismically imaged structures near the CMB span a wide range of sizes, from ~5000-km LLSVPs at one end (15, 16) to ~100-km ULVZs on the other (3, 17). So-called “mesoscale” structures have also been documented, including the Perm (16) and Kamchatka

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**Fig. 1. Postcursors across the northern Pacific.** A comparison of the source deconvolved Sdiff waveforms of moment magnitude ($M_w$) > 6.5 deep earthquakes (depth > 200 km) between 100° and 110° epicentral distance sorted by (A) distance and (B) the Sequencer. Sequencer ordering enables the identification of a substantial (~40% of all waveforms) subpopulation of Sdiff postcursors [red box in (B)]. (C) Histogram of fraction of waveforms with postcursors in 1° radius bins (bottom) and the geographic locations (top) where postcursors are absent (peach), pervasive (cyan), and exclusive (pink). (D) Stacks of post-cursor amplitude relative to main Sdiff arrival, also averaged in 1° bins. The geographic extent of the Pacific LLSVP (18) is shown (light-blue contour), as are the five largest hot spots by mass flux (black crosses) (35). The region with the strongest postcursors is outlined in red. Regions labeled R1 to R4 are discussed in the main text.
anomalies, as well as unusually large ULVZs (4, 6, 20). Therefore, we explored two types of candidate structures: (i) cylindrical regions of reduced or elevated shear-wave velocity \((V_S)\) with dimensions reminiscent of ULVZs and (ii) undulating boundaries of large low-\(V_S\) regions reminiscent of LLSVPs (Fig. 3). We explored the effects of the lateral abruptness of velocity changes across the boundaries of both types of structures.

Our waveform simulations confirmed that postcursors have origins from regions 20° away from a low-velocity cylinder (Fig. 3A, inset). The slope of this decay (Fig. 3) is controlled by the geographical pattern to the region northwest of Hawaii. Earthquakes and seismic stations are plotted as red stars and blue triangles, respectively. The geographic extent of the Pacific LLSVP (18) is shown (purple contour), as are the five largest hot spots by mass flux (black crosses) (35).

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incorporating the postcursor waveforms. Although more complicated models cannot be ruled out, such as a 100-km-tall extremely low $V_S$ (25% reduction) structure embedded in the northern edge of Pacific LLSVPs (7), we prefer the plume root structure to explain the amplitudes and waveforms of Hawaii postcursors.

Away from Hawaii and the Marquesas, postcursor amplitude (Fig. 4B, black) is constant with delay time and significantly greater (Fig. S10) than the largest post-Sdiff signal in waveforms that do not show a postcursor when sequenced (Fig. 4B, gray). Postcursor amplitudes cannot be attributed to deconvolution artifacts.

Fig. 4A. Comparison of observed postcursor delay time versus log amplitude trends with predictions for candidate lowermost mantle structures. (A) Log amplitudes decrease strongly with delay time for postcursors near Hawaii (filled circles) and Marquesas (open circles) hot spots, in agreement with predictions (dashed lines) for three cylindrical ULVZ models (red). The prediction for an ultrahigh-velocity zone (UHVZ) model is plotted in blue. Upper inset shows illumination geometry of synthetic waveforms calculated for the cylindrical ULVZ models. Lower inset shows Fig. 3A and the diffraction coverage of the dataset (black outline). (B) For pervasive postcursors, log amplitude is observed to be constant with delay time (black boxplots) and agrees with the postcursors predicted for waves traversing a sharp LLSVP boundary (5% $V_S$ contrast) edge-on (lavender). Head-on geometries (light blue) underpredict the amplitudes. Detection limit is defined by the 75th percentile of the post-Sdiff amplitude in nonpostcursor waveforms (outside the red box in Fig. 1B).
(10) (fig. S10). The spatial pattern of postcursors amplitudes variations has a characteristic length scale of ~3000 km (fig. S11), which is similar to the Fresnel width for a scattered arrival with a delay time of 30 to 50 s. We ruled out that the structure beneath Hawaii alone produces the postcursors observed across the northern Pacific, because our wavefield simulations indicate that regardless of height, this structure cannot produce postcursors of sufficiently large amplitude on paths >20° away from its center (fig. S8). Rather, two scenarios can plausibly explain postcursors identified by the Sequencer across the northern Pacific: (i) scattering from multiple smaller anomalies distributed across the region and (ii) scattering or multipathing across sufficiently laterally abrupt boundaries of the LLSVPs.

Multiple anomalies distributed across the Pacific could have complex geometries or comprise various ULVZs with various geometries and sizes (23). A conglomerate of individual ULVZs that are smaller than our wavelength and ubiquitous across the region may produce the pervasive postcursors we observed. Whether these anomalies involve partial melting (24) or compositionally distinct, low shear-wave pulses (Fig. 1B) that propagate from its center (fig. S8). Rather, two scenarios indicate that regardless of height, this structure has dimensions similar to the Fresnel width for a scattered arc (Fig. 4B, lavender) better reproduce observed amplitudes. The effects of impedance contrast (Fig. 4B, lavender) better reproduce observed amplitudes.

Incorporating higher-frequency waveforms would enable us to constrain structures of even smaller scale. These waveforms are harder to interpret but should not pose a challenge to our manifold learning approach. Our wavefield simulations indicate that, given their frequency content (15 to 100 s), our data cannot resolve velocity variations at scales smaller than ~50 km. Although geometry of seismic illumination to the lowermost mantle will remain more or less the same, Sequencer-based approaches for identifying trends and anomalous signals in portions of seismograms that host various seismic phases will advance our understanding of deep Earth structures.

Our systematic postcursor search in the Pacific basin, interpreted with insights from waveform simulations, reveals that heterogeneity capable of producing postcursors is widespread in the CMB region. We found that strong postcursors exhibit an anticorrelation between delay time and log amplitude that can be detected locally. The two strongest postcursor signals in the Pacific are related to the Marquesas and a broad region near Hawaii. The previously unknown localized anomaly near the Marquesas has dimensions similar to that of a mega-ULVZ (4). The anomaly beneath Hawaii is unique in the Pacific basin, producing postcursors that can only be explained by a structure either substantially larger than a mega-ULVZ or by a plume conduit. Weaker postcursors are observed throughout the Pacific basin and do not exhibit a correlation between delay time and amplitude; they are best explained by scattering from laterally abrupt edges of LLSVPs (5% V_s contrast). The origins of and relationships among these CMB region structures remain controversial (31). Nevertheless, recent analyses suggest that LLSVPs may host relatively undegassed geochemical reservoirs (32). Mega-ULVZs, on the other hand, must involve either exotic compositions or reflect the presence of partial melt (24, 33), and they have been proposed to host primitive geochemical signatures predating the moon-forming impact (34). Therefore, our discovery of a mega-ULVZ beneath the Marquesas offers a test of this hypothesis.
All authors helped edit the manuscript. Competing interests: The authors declare no competing interests. Data and materials availability: Seismic data used in this manuscript are available through the IRIS Data Management Center (DMC). The source code of the Sequencer, together with implementation details, can be found at https://github.com/dalya/Sequencer/. An online version of the algorithm is available at http://sequencer.org.

SUPPLEMENTARY MATERIALS
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Materials and Methods
Figs. S1 to S16
References (36–44)

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