An overview of asphalt pavement design for streets and roads

Descripción general del diseño de pavimentos asfálticos para calles y carreteras

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ABSTRACT: Pavements constitute a geotechnical problem since they are built on the ground and with materials obtained from it: untreated, such as soils and rocks, and processed as hydraulic and bituminous binders; consequently, a geotechnical framework is useful to describe their constitutive elements. The design of asphalt pavements for streets and roads evolved from empirical to mechanistic-empiric (M-E) procedures throughout the 20th century. The mechanistic-empiric method, based on layered elastic theory, became a common practice with the publication of separate procedures by Shell Oil, Asphalt Institute, and French LCPC, among others. Since its origin, the M-E procedure can consider incremental pavement design but, only until the beginning of the 21st century, the computational power became available to practicing engineers. American MEPDG represents the state-of-the-art M-E incremental design procedure with significant advantages and drawbacks, the latter mainly related to the extensive calibration activities required to assure a proper analysis and design according to subgrade, climate, and materials at a particular location and for an intended level of reliability. Perpetual pavements are a subset of M-E designed pavements with a proven history of success for the conditions where they are warranted. No design method, either the most straightforward empirical approach or the most elaborated incremental mechanistic one, is appropriate without proper knowledge about the fundamental design factors and calibration of the performance models for each distress mode upon consideration.

RESUMEN: Los pavimentos constituyen un problema geotécnico pues se construyen sobre el terreno con materiales obtenidos del mismo: no tratados, como suelos y rocas, y procesados como los aglomerantes hidráulicos y bituminosos; en consecuencia, el marco de referencia geotécnico es útil para describir sus elementos. El diseño de pavimentos asfálticos evolucionó de procedimientos empíricos a mecanicistas-empíricos (M-E) durante el siglo veintiuno. El método mecanicista-empírico, basado en la teoría de capas elásticas, se convirtió en una práctica con la publicación de los procedimientos de la Shell Oil, el Asphalt Institute y el LCPC, entre otros. Desde su origen, el procedimiento M-E consideró el diseño incremental del pavimento, sin embargo, solo hasta comienzos del siglo veintiuno se dispuso de la potencia computacional necesaria. La MEPDG representa el estado del arte del diseño incremental con avances e inconvenientes significativos, estos últimos relacionados con las actividades de calibración requeridas para el adecuado análisis y diseño según la subrasante, clima y materiales del sitio y para un nivel requerido de confiabilidad. Los pavimentos perpetuos son un subconjunto diseñado con el método M-E y con una trayectoria exitosa para las condiciones en las cuales son apropiados. Ningún método de diseño, desde la aproximación empírica más sencilla hasta el más complejo método mecanicista incremental, es adecuado sin un conocimiento satisfactorio de los factores de diseño y la calibración de los modelos de comportamiento para cada modo de daño.
1. Introduction

Asphalt pavements are made up of multiple layers: subgrade, unbound subbase and base, hydraulic-binder or asphalt-treated bases, asphalt concrete bases, and wearing courses. All these materials show a complex response to load and environmental changes. Each region or country may follow a particular pavement design guide, but they all must conform to the same basic design principles: considering load repetitions and environmental cycles, and relating the theoretical and the real behavior of materials and structures [1]. Traffic characterization and forecasting, pavement materials and subgrade assessments, environmental effects, and life-cycle economic analysis are challenging in all pavement projects regardless of their longitude, intended purpose (road, port, or airport), and strategic value (local, collector or highway). This article presents an overview of asphalt pavement design for streets and roads, divided into four sections; this Introduction is the first one. The second section introduces the geotechnical framework and the design principles of asphalt pavements in streets and roads. The third section summarizes the evolution of the structural design of asphalt pavements from the empirical approaches to the current mechanistic-empirical methodologies, and the fourth section summarizes the views of the authors about the subject.

2. The geotechnical framework and the design principles of asphalt pavement design

Pavements constitute a geotechnical problem since they are built on the ground and with materials obtained from it: untreated, such as soils and rocks, and processed as hydraulic and bituminous binders. People built pavements over the terrain, on cuts, embankments, even inside tunnels, or at the bottom of human-made ponds. Pavement materials include natural and artificial constituents as soil, rock, lime, Portland cement and bitumen, polymers and geo-synthetics, and a variety of chemical products to enhance their natural characteristics. Even though pavement failure usually does not compromise life or property, pavements are challenging structures and require a systemic approach to include all the activities related to analysis, design, construction, and monitoring. Pavement management systems or modern asset management systems also include the economic aspects of pavement engineering [2].

Figure 1 shows the five constitutive elements of pavement as a geotechnical problem. This article focuses on the “Design” of asphalt pavements for streets and roads, the evolution of the design methods, and the current trends.

Pavement design consists of two broad categories: (a) design of asphalt mixtures and hydraulic-binder-treated materials, and (b) structural design of the pavement components, which is different from the structural design of bridges and buildings since environmental factors greatly influence the pavement structure. Serviceability and the intended use of the pavement are the main topics in designing a pavement structure [3].

Pavement design must consider the expectations of the users since the dynamic interaction between the vehicle and the pavement substantially affects their valuation of the structure. The design of functional pavements must focus on the satisfaction of the users considering five primordial aspects: velocity, smoothness, safety, maintenance, and cost. Therefore, a systematic approach to pavement design must consider the “optimization of the pavement” when all the components (subgrade, structure, wearing course) have the same structural reliability, including their general response to environmental conditions. The design problem has a cost associated with reliability, which also affects the construction, maintenance, operation, and contingency costs in the life cycle of the project [4].

3. Evolution of the asphalt pavement design methods for streets and roads

The structural design of pavements evolved from “art to science” however, empiricism is indispensable to calibrate the behavior of in-service structures with the responses of the analytical models. The modern asphalt pavements appeared at the end of the nineteenth century, built by combining techniques developed a century before with innovative materials in the upper layers to water-proof the structure and control the dust production. Pavement design methods comprise two main groups: empirical methods and mechanistic-empirical methods, also called analytical or rational methods [5].

3.1 Empirical methods

The empirical methods include those based on the subgrade engineering classification (Bureau of Public Roads), the relative shear resistance of the soil (CBR), and road experiments such as the WASHO Road Test (1952-1955) and the AASHO Road Test (1958-1962). The design method considers the observed behavior of in-service pavements under traffic, environmental, and
The method based on the California Bearing Ratio test

The method based on the CBR test (ASTM D1833) began with the work in Soil Mechanics in the California State Highway Division. Later on, the United States Army Corps of Engineers (USACE) developed Equation 1 to correlate the CBR, the pavement thickness, and the magnitude of the wheel load based on calibration studies during World War II [7].

$$T = \sqrt{P \left( \frac{1}{8.1 \cdot CBR} - \frac{1}{q \cdot \pi} \right)}$$  \[1\]

Where $T$ is the total thickness of the pavement in inches (1 inch = 25.4 mm), $P$ is the applied wheel load in pounds (1 lb = 4.4482 newtons), $CBR$ is the California Bearing Ratio in percent, and $q$ is the tire pressure in psi (1 psi = 6.8948 kPa).

Figure 2 shows the evaluation of Equation 1 for three levels of wheel load and tire pressure of 224 psi (1682 kPa), which represents the landing gear of a World War II bombardier.
In the CBR method, pavement fails because of permanent deformation due to excessive shear stresses in the subgrade. Therefore, the design principle of the CBR method is to protect the subgrade with a minimum thickness of material with better quality than the on-site soil. The main limitation of the CBR method is that it does not take into account the strength of the upper layers in the pavement structure. After the publication of the AASHO Road Test results, Road Agencies modified the CBR method to characterize the vehicular traffic as repetitions of an 18-kips standard single axle based on several assumptions [8].

Figure 3 shows the 1979 National Association of Australia State Road Authorities (NAASRA) pavement design method for traffic intensities up to 50 million repetitions of the AASHTO standard axle of 80 kN and CBR values between two and 30 percent. Later on, Austroads updated this chart to design pavements with thin asphalt surfacing [9].

American Association of State Highways and Transportation Officials method

The AASHTO method is based on the statistical analysis of pavement behavior data obtained in the AASHO Road Test (1958-1960), a full-scale facility built in Ottawa, IL. (USA). Although the origin of the method has a robust empirical component, its successive versions incorporated mechanistic analysis to interpret and extrapolate the results from the Road Test on asphalt pavements. In the latest version, the design method incorporated mechanistic concepts into a “semi-empirical” approach that considers two design criteria: serviceability and reliability [10].

Serviceability, or Present Serviceability Index (PSI), was developed in the 1950s from the subjective evaluation of multiple pavement sections with the Present Serviceability Rating and its statistical correlation with measurable characteristics like roughness and distress (cracking, deformation, patching).

Theoretically, PSI varies between zero (a failed pavement) and five (a good pavement); however, the AASHO Road Test data indicates that asphalt pavements may be in the range from 4.2 to 1.5 or less. Equation 2 shows the original relationship between the PSI and several measurable characteristics of asphalt pavements:

\[
PSI = 5.03 - 1.91 \times \log_{10} (SV + 1) - 1.38 \times RD^2 - 0.01 \times \sqrt{C + P} \tag{2}
\]

Where \(RD\) is the average rut depth in inches (1 inch = 25.4 mm) on both wheel tracks, and SV is the slope variance of the average slope of both wheel tracks \(\times 10^6\) measured with the CHLOE profilograph. \(C\) is the cracked area with an alligator pattern, and \(P\) is the patched area, both in square feet over 1,000 ft\(^2\) (1 ft\(^2\) = 0.0929 m\(^2\)).

Roughness has a significant effect on PSI, and, at present, it is represented as the effect of the road profile over a standard vehicle, i.e., the International Roughness Index (IRI). For example, Figure 4 shows three correlations between PSI and IRI that substitute the use of Equation 2.

Reliability considers two sources of uncertainty in pavement design: (a) the prediction of the future traffic on the structure, and (b) the prediction of the serviceability of the pavement in any future moment after supporting the traffic loading. Both uncertainties are standard deviations of the logarithm of the accumulated standard 18-kip...
single-axle loads. Thus, the overall standard deviation ($S_o$) is given by Equation 3:

$$S_o = \sqrt{S_w^2 + S_n^2}$$  \[3\]

Where $S_w$ is the standard deviation of the traffic estimation and $S_n$ is the standard deviation of the pavement condition assessment.

Figure 4 PSI versus IRI empirical relationships. Redrawn from [11, 12]

The structural design of asphalt pavements with the 1993 AASHTO method applies the pavement behavior algorithm given by Equation 4 [10]:

$$\log_{10}(W_{18}) = Z_r \cdot S_o + 9.36 \cdot \log_{10}(SN + 1) - 0.20 + 2.32 \cdot \log_{10}(M_r) - 8.07$$  \[4\]

Where $W_{18}$ is the expected number of repetitions of the standard single axle load of 18-kips on the design lane for the design period of analysis; $Z_r$ is the accumulated value of the standardized normal distribution for a given reliability level; $S_o$ is as previously defined in Equation 3; $SN$ is the "structural number", an abstract representation of the pavement equal to the summation of the products of the layer thickness ($D_i$, in inches) times a non-dimensional coefficient that represents the layer quality ($a_i$), $[SN = \sum D_i \times a_i]$; $\Delta PSI$ is the estimated loss of serviceability in the service period; and $M_r$ is the resilient modulus of the pavement materials or subgrade in psi ($1 \text{ psi} = 6.8948 \text{ kPa}$).

Figure 5 shows a design chart for flexible asphalt pavements with a reliability of 50%. The chart includes three values of resilient moduli of the subgrade: 1,500 psi, 3,000 psi, and 6,000 psi. The properties of the materials are summarized in the same chart. The thicknesses are in millimeters to ease comparison with Figure 3. The increase in layer thickness follows the same tendency for the method based on the CBR test. There are some discontinuities in the granular subbase thickness curves due to the minimum requirements of thicknesses for the asphalt and granular base layers in the AASHTO method.

Figure 5 Flexible pavement design chart based on the 1993 AASHTO method

Engineers still use the 1993 AASHTO method in the design of both new pavements and the rehabilitation of existing ones. However, part of the design practice is based only on the CBR test, and practitioners apply the AASHTO method with several uncertain presumptions and correlations for local or regional conditions.

3.2 Mechanistic-empirical methods

Method of analysis

The mechanistic-empirical method became useful with the introduction of the layered elastic theory in 1943 [13]. However, only until the 1962 "First International Conference on the Structural Design of Asphalt Pavements", the theory gained attention as a valid method of analysis for pavements [14]. The initial application of layered elastic theory considered systems with two or three layers simplified in tables and charts [3]. The two and three-layers solutions focused on measurable structural responses calibrated with the in-service behavior of asphalt pavements as the surficial deflection or the vertical stress. The analysis of road and airfield pavements extensively uses the layered elastic theory (LET). LET models the structure as a semi-infinite continuum, divided into layers of finite thickness over an elastic half-space, as shown in Figure 6.

LET employs boundary pressures to simulate the effect of wheel loads. Early works computed the vertical stresses under parabolic loads with superposition to overcome the inaccuracy of constant contact pressures [15]. The extension of the LET differential equations
allows considering vertical, centripetal-horizontal, unidirectional-horizontal, and rotational-horizontal loads [16]. A uniformly distributed rectangular model, with normal and shear components, is a more realistic approach to the tire footprint according to the tensile-strains in the asphalt concrete and compressive-strains in the subgrade [17]. Besides the load representation, there are proven issues about the capacity of LET to represent real stresses and strains in pavements [18].

Alternatives for the layered elastic theory

Method of equivalent thickness: The method of the equivalent thickness (MET) allows the fast computation of responses by transforming a multi-layered media to a single layer with a transformed thickness increased (or decreased) by a factor near to the one-third power of the modular ratio. The method assumes the equality of the rigidity against flexural stress with adjustment factors for better agreement with layered elastic solutions [19].

Probabilistic stress distribution: This method predicts the stress distribution in flexible pavements with the central limit theorem of probability and a coefficient of lateral stress for each material. The linear-elastic solution is a particular case of this approach without assumptions about the transference of boundary energy at the interfaces [20].

Supervised learning algorithms: Artificial neural networks (ANN) and support vector machines (SVM) can estimate the tensile strain in asphalt layers and compressive strain in the subgrade under a standard axle load of 80 kN. Both techniques give coefficients of determination higher than 0.99 in training and testing tests with a synthetic database of N-layer LET solutions [21, 22].

Finite element method (FEM): The layered theory has limitations such as the inability to capture the exact load geometry and boundary conditions. The evaluation of 2D, axisymmetric, and 3D FEM computations indicates that axisymmetric models give a reasonable solution in terms of computation time and capabilities to problems unaffected by boundary or discontinuity conditions [23]. The main advantage of FEM is that it considers elastic non-linear or viscoelastic materials, as well as complex load conditions. The disadvantages are that FEM requires more computational processing time and more information about the behavior of the materials.

The method of analysis is not the pavement design procedure by itself. In pavement design, the challenges are in the mechanical characterization and calibration of the behavior of the materials with real-life conditions.

The basis of the conventional mechanistic-empirical design

The fundamental principles of the structural design of asphalt pavements consider two primary modes of distress:

Permanent deformation: Permanent, plastic, or irrecoverable deformation of the pavement structure appears in the surface as ruts or surface depressions in the trajectory of the wheels. This damage, known as “rutting” [24], is due to two leading causes: (1) the plastic deformation of the unbounded materials due to the change in volumetric phases by secondary compaction under traffic, or by general shear failure in the foundation soil; (2) the plastic deformation of asphalt mixes with excessive amounts of binder or subjected to high temperatures.

Rutting is a compound failure mode; however, there is an empirical model that relates the unrecoverable surface deformation with the elastic response of the subgrade defined by Equation 5:

$$N_d = \frac{k_4}{\varepsilon_z k_5}$$

Where $N_d$ is the allowable number of load repetitions until the development of a rut of a certain depth, and $\varepsilon_z$ is the vertical compressive strain at the top of the subgrade due to the traffic loading. The values $k_4$ and $k_5$ are obtained with regression analysis from the observation of in-service pavements. There is a substantial dispersion in the published models because of the differences in the rut depth defined as failure threshold and the discard of the real contribution of each layer to the total plastic deformation of the pavement. At present, it is accepted that the rutting estimation in all the layers of the pavement must be part of any rigorous mechanistic-empirical design.
Fatigue cracking: Fatigue cracking is a series of interconnecting cracks caused by fatigue failure of the asphalt concrete surface under repeated traffic loading [24]. The properties of asphalt materials change throughout the service life of the pavement with the aging of the bitumen caused by environmental conditions. Materials treated with hydraulic binders (Portland cement, lime, fly ash, and slag) also present changes in their mechanical properties throughout the service life. The traditional fatigue model considers that cracking starts in the bottom of layers due to tensile stresses under traffic loading, i.e., "bottom-up cracking"; however, research indicates that fatigue cracking tends to develop from top to bottom, or "top-down", and that the opposite is less frequent on in-service pavements [26].

The horizontal tensile strain correlates with the fatigue behavior of the asphalt layers and depends primarily on the layer thickness and the rigidities of the asphalt and base layers. Equation 6 represents the fatigue behavior of asphalt materials:

\[ N_{\text{failure}} = C_f \cdot \frac{k_1}{\varepsilon_t} k_2 \cdot E_{ka} \]  

Where \( N_{\text{failure}} \) is the number of load repetitions to fatigue failure of the asphalt material subjected to a repetitive horizontal strain \( \varepsilon_t \) at a temperature and load conditions that mobilize a specific Young’s modulus \( E \). The values \( k_1, k_2 \) and \( k_3 \), are obtained from laboratory fatigue tests and the \( C_f \) coefficient calibrate the controlled conditions in the laboratory with the real behavior of in-service pavements.

The general procedure of the mechanistic-empirical design

Figure 7 shows a flowchart for a mechanistic-empirical (M-E) pavement design procedure with multiple seasons (climatic sub-periods) and several load groups.

The conventional M-E design considers one season, with weighted or critical climatic values, and a single load group of repetitions of a standard axle. The consideration of multiple climatic seasons and several load groups by type (single, tandem, triple, and quad) and magnitude (load spectra) defined the basis of the incremental design method even before the development of the MEPDG.

The following paragraphs present some general aspects of two classic M-E methodologies, Shell Oil and the French Design Method, and the basics of the MEPDG for flexible pavements. The influence of the latter methodology is growing in practice despite its demands for extensive activities of calibration and materials characterization.

Shell Oil method: The first edition of the Shell method dates from 1963. Later on, the “Shell Pavement Design Manual (SPDM)” of 1978 and its 1985 addendum replaced it. The method is based on the layered elastic theory and presents the design alternatives in charts and tables. The last version of the Shell method, known as SPDM 3.0, is a software suite published in 1993 without any known updates to date [27].
a. Fatigue of bituminous mixtures based on constant stress tests:

\[
\varepsilon_t = \frac{[36.43 \cdot PI - 1.82 \cdot PI \cdot V_b + 9.71 \cdot V_b - 24.04]}{10^6} \cdot \left(\frac{S_m}{5 \times 10^9}\right)^{-0.28} \cdot \left(\frac{N_f}{10^6}\right)^{-0.20} \tag{7}
\]

b. Fatigue of bituminous mixtures based on constant strain tests:

\[
\varepsilon_t = \frac{[36.43 \cdot PI - 1.82 \cdot PI \cdot V_b + 9.71 \cdot V_b - 24.04]}{10^6} \cdot \left(\frac{S_m}{5 \times 10^{10}}\right)^{-0.36} \cdot \left(\frac{N_f}{10^6}\right)^{-0.20} \tag{8}
\]

In both Equations 7 and 8, \(\varepsilon_t\) is the tensile strain, \(PI\) is the bitumen penetration index, \(V_b\) is the percentage of bitumen volume in the mix, \(S_m\) is the stiffness modulus of the mix in N/m², and \(N_f\) is the number of repetitions to failure. Equation 9 defines the penetration index of the bitumen (PI):

\[
PI = \frac{20 - 500 \cdot A}{1 + 50 \cdot A} \tag{9}
\]

Where \(A\) is the temperature susceptibility of the bitumen, i.e., the slope of the line plot between the logarithm of penetration (pen = 0.1 mm) and temperature (°C) as defined by Equation 10:

\[
A = \frac{\log \text{pen at } T_1 - \log \text{pen at } T_2}{T_1 - T_2} \tag{10}
\]

c. Rutting associated with the subgrade response as given by Equation 11:

\[
N_d = 6.15 \times 10^{-7} \cdot (\varepsilon_c)^{-4.00} \tag{11}
\]

Where \(N_d\) is the number of load repetitions to failure, defined as a 13 mm rut depth, with a reliability of 50% reliability, and \(\varepsilon_c\) is the vertical compressive strain at the top of the subgrade.

Figure 8 shows a design chart based on the Shell procedure for structures on a subgrade with Young’s modulus of 50 MPa and a weighted mean annual air temperature of 20°C. The asphalt mix has the mechanical properties of a dense-graded mix or S1-F1-100 in Shell codification.

The horizontal axis represents the thickness of untreated base layers, and the vertical axis represents the thickness of the asphalt concrete layers. The chart includes nine traffic levels of repetitions of the 80 kN axle load. The rutting controls the structures with small thicknesses of unbound base and asphalt while the fatigue of the asphalt mix controls the thicker ones.
kPa. Equation 12 is used to transform any axle to the standard axle [29]:

$$A = K \cdot \left( \frac{P}{130kN} \right)^{\alpha}$$  \hspace{1cm} (12)

Where $A$ is the "aggressiveness" of any given axle, $K$ is used to take into account the kind of axle, $P$ is the axle weight in $kN$, and $\alpha$ is a function of the type of material and structure. Table 1 summarizes the values of $\alpha$ and $K$ for French conditions on regular and highly trafficked new flexible and semi-rigid pavements.

Equations 13 to 17 summarize the design criteria of the French method [28] and [29]:

a. Fatigue of bonded or cemented materials: For asphalt pavements, the allowable strain is defined by Equation 13:

$$\varepsilon_{t,ad} = \varepsilon_6 \left( 10^6 \theta \right) \cdot \sqrt[2]{\frac{E(10^6)}{E(\theta_{eq})}} \cdot \left( \frac{NE}{10^6} \right)^b \cdot k_r \cdot k_c \cdot k_s$$  \hspace{1cm} (13)

Where $\varepsilon_{t,ad}$ is the allowable tensile strain in the asphalt layer; $\varepsilon_6 (10^6 \theta)$ is the tensile strain of the fatigue law at $10^6$ cycles; $E(10^6)$ is the elastic modulus of the asphalt mixture at the equivalent temperature ($\theta_{eq}$); $NE$ is the number of load repetitions to failure with a 50% probability, and $b$ is the slope of the bi-logarithmic fatigue law. For pavements with hydraulic-binder-treated bases or concrete slabs, the allowable stress is defined by Equation 14:

$$\sigma_{t,ad} = \sigma_0 \cdot (1 + 6\beta) \cdot \left( \frac{NE}{10^6} \right)^b \cdot k_r \cdot k_d \cdot k_c \cdot k_s$$  \hspace{1cm} (14)

Where $\sigma_{t,ad}$ is the allowable tensile stress at the bottom of tensile-stressed layers; $\sigma_0$ is the indirect tensile strength of the material; $\beta$ is the slope of the Wohler’s curve [$\sigma/\sigma_0 = 1 + \beta \cdot \log N$]; $NE$ is the number of load repetitions to failure with a 50% probability; and $b = -0.5 \cdot \log \left( \frac{1+5\beta}{1+7\beta} \right)$ for load repetitions between $10^5$ and $10^7$. In Equations 13 and 14, the coefficients $k_r$, $k_c$, $k_s$, and $k_d$ modify the allowable strain or stress considering the reliability, the type of pavement, the modulus of the subgrade, and the type of materials treated with hydraulic binders, respectively. The following paragraphs present their definitions.

The coefficient $k_r$, defined in Equation 15, adjusts the allowable strain or stress values to the design reliability:

$$k_r = 10^{-Zr \cdot b \cdot \delta}$$  \hspace{1cm} (15)

Where $Z_r$ is the accumulated value of the standardized normal distribution for a given reliability (or risk) level, $b$ is the slope of the bi-logarithmic fatigue law, and $\delta$ is the standard deviation associated with the load repetitions given the dispersion of the fatigue law and the layer thickness as shown in Equation 16:

$$\delta = \sqrt{SN^2 + \left( c \cdot Sh \cdot b \right)^2}$$  \hspace{1cm} (16)

Where $SN$ is the standard deviation of the logarithm of the number of cycles at failure, $Sh$ is the standard deviation of the layer thickness, $c$ is the coefficient linking the variation in strain or stress to the random variation in thickness ($\log \varepsilon = \log \varepsilon_{eq} - c \cdot \Delta h$), and $b$ is the slope of the bi-logarithmic fatigue law.

The calibration coefficient $k_c$ adjusts the allowable strain or stress to the performance observed on pavements of the same type. The coefficient $k_s$ is a reducing factor that takes into account the heterogeneity of the bearing capacity of the roadbed. The coefficient $k_d$ takes into account the effect of joints or shrinkage cracks in cement-treated materials or concrete slabs. Table 2 summarizes the suggested values of the coefficients for French conditions.

b. The rutting associated with the untreated layers is evaluated with Equation 17:

$$\varepsilon_{z,ad} = A_r \cdot (NE)^{-0.222}$$  \hspace{1cm} (17)

Where $\varepsilon_{z,ad}$ is the allowable compressive strain on the top of untreated or subgrade layers; $A_r$ is 0.012 in pavements with medium or high traffic and 0.016 in pavements with low traffic, and $NE$ is the number of load repetitions to failure.

| Type of structure | Parameter $\alpha$ | Parameter $K$ |
|-------------------|-------------------|---------------|
| Flexible and bituminous pavements | 5 | 1 | 0.75 | 1.1 |
| Semi-rigid pavements | 12 | 1 | 12 | 113 |
Table 2 Coefficients for calculation of allowable strains and stresses [28]

| Coefficient | Pavement material                        |
|-------------|------------------------------------------|
| $k_c$       | Semi-coarse graded aggregate base asphalt concrete | Asphalt concrete | High modulus asphalt concrete | Cement-treated graded aggregates | Cement concrete and slag treated graded aggregates |
|             | 1.3                                       | 1.1              | 1.0                          | 1.4                          | 1.5                      |
| $k_s$       | Subgrade modulus                         | E $<$ 50 MPa     | 50 MPa $\leq E \leq$ 120 MPa | E $>$ 120 MPa                | 1.0                      |
|             | 1 / 20                                    | 1 / 1.10         | 1 / 20                       | 1 / 1.10                     | 1 / 1.10                 |
| $k_d$       | Pavement material                         | Treated gravels class G2 and G3 | Treated gravels classes G4 and G5 and rolled concrete | Un-dowelled cement concrete slabs | Dowelled cement concrete slabs | Continuously reinforced concrete |
|             | 1.0                                       | 1 / 1.25         | 1 / 1.27                     | 1 / 1.10                     | 1 / 1.10                 |

The French pavement design method "is the most comprehensive design method in use in Europe", [30] and its suitability to any local practice depends on the field calibration and the adoption of construction specifications that evaluate the mechanical performance of the materials. Figure 9 shows the ideal design procedure proposed by the "Advanced Models for Analytical Design of European Pavement Structures – AMADEUS" report. The incremental European approach anticipated the MEPDG by several years; however, it is not implemented to date.

Mechanistic-Empirical Pavement Design Guide (MEPDG): The MEPDG is the main product of the NCHRP 1-37A project for the implementation of mechanistic-empirical pavement analysis and design procedure. A mechanic model computes structural responses that consider material properties, environmental conditions, and loading-characteristics of the vehicles. The structural responses are analyzed with empirical models to evaluate the performance and predict the distress of the pavement. The accuracy of the empirical models to predict damage depends on the quality of the field data obtained to calibrate them [25].

Figure 10 shows the conceptual schematic of the design process of MEPDG divided into three stages: evaluation, analysis, and strategy selection.

The method considers two types of models: one that directly predicts the damage (rutting), and one that predicts the damage from calibrated observations (fatigue). The design process differs from conventional methods because the result is the estimated distress of the structure and not the thicknesses of the layers.

The MEPDG considers three hierarchical levels for the input data: The Level 1 demands high-quality laboratory characterization of the materials, the Level 2 uses correlations between simple parameters and advanced material characterization, and the Level 3 uses local or national values by default. The hierarchical level must coincide with the relevance of the project. The initial calibration of the method corresponds to Level 3, and, in consequence, the road agencies must develop local studies [32].

Figure 9 Flowchart of an incremental pavement design procedure [31]
The method of analysis is the layered elastic theory, based on the JULEA program, except for non-linear analysis in the hierarchical Level 1 that uses the finite element method with the DSC2D program. The traffic loading characterization uses load spectra of single, tandem, triple, and quad axles with multiple analysis points in the pavement structure to obtain the critical responses, as shown in Figure 11.

The incremental damage analysis divides the design period into sub-periods of one month or even two weeks. In each sub-period, all the layers support the predicted traffic under the predominant weather and materials conditions. The damage is accumulated to predict the progressive deterioration of the structural and functional conditions.

The MEPDG can consider a wide range of materials: Hot mix dense-graded asphalt concrete, asphalt-treated open-graded permeable base materials, cold mix asphalt, Portland cement concrete, cement-treated or lean concrete base, cement-treated open-graded permeable base materials, untreated base materials (granular base or granular subbase), lime modified or stabilized soils, subgrade soil, and bedrock.

For hot-mix-asphalt-surfaced pavements, the specific performance models are [25] and [33]:

1. Total rut depth and rutting in hot-mix asphalt, unbound aggregate base, and subgrade.

   a. Plastic deformation for hot-mix asphalt (HMA) computed by Equation 18:

   \[
   \Delta p(HMA) = \left[ \beta_{1r} \cdot k_z \cdot \varepsilon_r(HMA) \cdot 10(k_1r) \right] \\
   \cdot (h_{HMA}) \cdot \left[ n(k_{2r} \cdot \beta_{2r}) \right] \\
   \cdot \left[ T(k_{3r} \cdot \beta_{3r}) \right] \tag{18}
   \]

   Where \( \Delta p(HMA) \) is the accumulated plastic vertical deformation in the HMA layer (in.); \( \varepsilon_r(HMA) \) is the resilient strain calculated at the mid-depth of the HMA layer (in./in.); \( h_{HMA} \) is the thickness of the HMA layer (in.); \( n \) is the number of axle-load repetitions; \( T \) is the pavement temperature (°F); \( k_z \) is the depth confinement factor; \( k_{1r} \), \( k_{2r} \), and \( k_{3r} \) are the global field calibration parameters (\( k_{1r} = -3.35412, k_{2r} = 0.4791, k_{3r} = 1.506 \)); and \( \beta_{1r}, \beta_{2r}, \) and \( \beta_{3r} \) are local field calibration constants (1.0 by default). The depth confinement factor is computed by Equation 19:

   \[
   k_z = (C_1 + C_2 \cdot D) \cdot (0.328196)^D \tag{19}
   \]

   Where the coefficients \( C_1 \) and \( C_2 \) are given by Equations 20 and 21:

   \[
   C_1 = -0.1039 \cdot (H_{HMA})^2 \\
   + 2.4868 \cdot (H_{HMA}) \\
   - 17.342 \tag{20}
   \]

   \[
   C_2 = 0.0172 \cdot (H_{HMA})^2 \\
   - 1.7331 \cdot (H_{HMA}) \\
   + 27.428 \tag{21}
   \]
b. Plastic deformation for unbound pavement layers and the foundation or embankment soil computed by Equation 22:

$$\Delta_{p(\text{soil})} = \left[ \beta_{s1} \cdot k_{s1} \cdot \varepsilon_v \right] \cdot \left[ \left( \frac{\varepsilon_0}{\varepsilon_r} \right) \cdot e^{-\left( \frac{\varepsilon_0}{\varepsilon_r} \right)} \right] \cdot h_{\text{soil}} \quad [22]$$

Where $\Delta_{p(\text{soil})}$ is the plastic deformation of the layer (in.); $n$ is the number of axle-load repetitions; $\varepsilon_0$ is the intercept determined from laboratory repeated load permanent deformation tests (in./in.); $\varepsilon_r$ is the resilient strain imposed in the laboratory to obtain material properties $\varepsilon_0$, $\varepsilon_r$, and $\rho$ (in./in.); $\varepsilon_v$ is the calculated average vertical resilient strain in the layer (in./in.); $h_{\text{soil}}$ is the thickness of the unbound layer (in.); $k_{s1}$ is a global calibration factor [$k_{s1} = 1.673$ (granular material), $k_{s1} = 1.350$ (fine soil)]; and $s_1$ is a local calibration constant (1.0 by default). The models to estimate the parameters $\beta$, $[\varepsilon_0/\varepsilon_r]$, and $\rho$ are computed with Equations 23 to 27:

$$W_c = 51.712 \left[ \left( \frac{M_r}{2555} \right)^{0.136} \right]^{-0.3586 \cdot (GWT)^{0.1192}} \quad [23]$$

$$\beta = 10^{-0.61119 - 0.017683 \cdot (w_c)} \quad [24]$$

$$C_0 = \ln \left[ \frac{a_1 \cdot (M_r)^{b_1}}{a_g \cdot (M_r)^{b_0}} \right] \quad [25]$$

$$\rho = 10^{9} \cdot \left[ \frac{C_0}{1 - (10^9)^{\beta}} \right]^{\frac{1}{2}} \quad [26]$$

$$\left( \frac{\varepsilon_0}{\varepsilon_r} \right) = 10^{\left[ (\rho) \cdot a_1 \cdot (M_r)^{b_1} \right] + \left[ (\rho/10^9) \cdot a_g \cdot (M_r)^{b_0} \right]} \quad [27]$$

2. Load-related alligator cracking, or bottom-up cracking. The estimation of fatigue damage is based on Miner’s law, given by Equation 29:

$$D = \sum_{i=1}^{T} \frac{N_i}{N_i^T} \quad [29]$$

Where $D$ is the damage; $T$ is the total number of analysis periods; $N_i$ is the actual traffic for period $i$; and $N_i$ is the traffic allowed under conditions prevailing in period $i$. The allowable number of axle-load applications needed for the incremental damage index approach to predict alligator and longitudinal fatigue cracks is given by Equation 30:

$$N_f(HMA) = k_f1 \cdot 10^{4.84 - \left( \frac{V_{ae}}{V_{ae} + 1} \right) - 0.69} \cdot C_H \cdot \beta f_{1} \cdot \left( \varepsilon_t \right)^{k_f2 \cdot \beta f_2} \cdot \left( E_{HMA} \right)^{k_f3 \cdot \beta f_3} \quad [30]$$

Where $N_f(HMA)$ is the allowable number of axle-load applications; $\varepsilon_t$ is the tensile strain at critical locations (in./in.); $V_{ae}$ is the effective asphalt content by volume (%); $V_a$ is the air voids by volume (%); $E_{HMA}$ is the dynamic modulus of the HMA measured in compression (psi); $k_{f1}$, $k_{f2}$, and $k_{f3}$ are the global field calibration parameters [$k_{f1} = 0.007566$, $k_{f2} = -3.9492$, $k_{f3} = -1.281$]; $\beta f_1$, $\beta f_2$ and $\beta f_3$ are local field calibration constants (1.0 by default). The thickness correction term ($C_H$) is dependent on the cracking type and for bottom-up cracking is given by Equation 31:

$$C_H = \frac{1}{0.000398 + \frac{1}{1 + e^{11.02 \cdot 0.000695 \cdot H_{HMA}}} \quad [31]$$

Where $H_{HMA}$ is the total thickness of the hot-mix asphalt (in). The final transfer function to calculate
alligator fatigue cracking from the fatigue damage is given by Equation 32:

$$\text{FC}_{\text{bottom}} = \left\{ \frac{6000}{1 + e^{[C_1 - C_1' + C_2 - C_2' \log_{10}(D - 100)]}} \right\} \cdot \left( \frac{1}{60} \right) \quad (32)$$

Where $\text{FC}_{\text{bottom}}$ is the bottom-up fatigue cracking [% of lane area]; $D$ bottom-up fatigue damage; $C_1 = 1.0$; $C_1' = (-2.0 \cdot C_2')$; $C_2 = 1.0$; $C_2' = -2.40874 - 39.748 \cdot (1 + H_{HMA})^{-2.856}$; and $H_{HMA}$ is the total thickness of the hot-mix asphalt [in.]

3. Load-related longitudinal cracking, or top-down cracking. The fatigue equation is the same as Equation 30, but the thickness correction term ($C_H$) is given by Equation 33:

$$C_H = \frac{1}{0.01 + \frac{12.0}{1 + e^{[10.675 - 2.8156 \cdot H_{HMA} - 12.0]}}} \quad (33)$$

Where $H_{HMA}$ is the total thickness of the hot-mix asphalt [in.]. The transfer function to calculate longitudinal fatigue cracking from the fatigue damage is given by Equation 34:

$$\text{FC}_{\text{top}} = \left\{ \frac{1000}{1 + e^{[7.003 - 3.50 \log_{10}(D - 100)]}} \right\} \cdot (10.56) \quad (34)$$

Where $\text{FC}_{\text{bottom}}$ is the top-down fatigue cracking (feet/mile); and $D$ top-down fatigue damage. The critical responses to compute fatigue are the surface of the pavement, 0.5 inches from the surface, and the bottom of each bound or stabilized layer.

The MEPDG also includes models to estimate non-load-related transverse cracking, fatigue cracking in chemically-stabilized bases, and reflective cracking in hot-mix asphalt overlays due to cracks and joints in existing flexible, semi-rigid, composite, and rigid pavements [33].

4. Smoothness (IRI) of pavements with unbound aggregate base and subbase. The IRI is estimated by Equation 35:

$$\text{IRI} = \text{IRI}_0 + 0.0463 \cdot \left[ \frac{\text{SF} \cdot \left( e^{\frac{\text{age}}{5}} - 1 \right)}{0.00119 \cdot (\text{TC}_L)_T + 0.1834 \cdot (\text{COV}_{RD}) + 0.00384 \cdot (\text{FC})_T + 0.00736 \cdot (\text{BC})_T + 0.00115 \cdot (\text{LC}_{\text{SNWP}})_{MH}} \right] \quad (35)$$

Where $\text{IRI}$ is the IRI at any given time [m/km]; $\text{IRI}_0$ is the initial IRI [m/km]; $\text{SF}$ is the site factor; $\text{age}$ is the age of pavement in years; $(\text{TC}_L)_T$ is the total length of transverse cracks [m/km]; $\text{COV}_{RD}$ is the coefficient of variation of the rut depths (assumed to be 20%); $(\text{FC})_T$ is the fatigue cracking in wheel path [% of total lane area]; $(\text{BC})_T$ is the area with block cracking as a percent of the total lane area [user input, not modeled by MEPDG]; and $(\text{LC}_{\text{SNWP}})_{MH}$ is the length of moderate and high severity sealed longitudinal cracks outside the wheel path in meter per kilometer [user input, not modeled by MEPDG]. The site factor is given by Equation 36:

$$\text{SF} = \left\{ \frac{(\text{RS}_D) \cdot (P_{075} + 1) \cdot (\text{PI})}{2 \times 10^4 \cdot \ln(FI + 1) \cdot (P_{02} + 1) \cdot \ln(R_m + 1)} \right\}$$

$$\quad \left\{ \frac{1}{10} \right\} \quad (36)$$

Where $\text{RS}_D$ is the standard deviation of the monthly rainfall (mm); $P_{075}$ is the percent passing the 0.075 mm sieve; $\text{PI}$ is the plasticity index of the soil [%]; $FI$ is the average annual freezing index [°C-days]; $P_{02}$ is the percent passing the 0.02 mm sieve; and $R_m$ is the average annual rainfall [mm].

The MEPDG also includes models to estimate the roughness progression in pavements with asphalt-treated and chemically-stabilized bases [33].

The method comprises equations to estimate the standard deviation of the predicted distresses and their confidence intervals to compute the reliability of the structural design. However, a review of the published comparisons between the measured and estimated distress shows that the proposed models are quite dispersed, with coefficients of correlation ($R^2$) of 0.577 for rutting, 0.275 for alligator cracking, 0.544 for longitudinal cracking, and 0.56 for IRI. Also, in the particular case of rutting, the "observed" values were proportionally distributed (not measured) between the layers from a single value of total superficial rutting [33].

In 2014, the NCHRP Synthesis 457 reported that 48 USA state highway agencies still used empirical design methods, three agencies implemented MEPDG (Indiana, Missouri, and Oregon), and 46 agencies had plans to implement the new method [34]. The implementation efforts in the USA and Canada report significant differences between the national and the local conditions, particularly about the sensitivity, bias, and standard error of the pavement distress models [35, 36]. Some local implementation programs include custom axle-load spectra, new analytical tools, and research on construction materials supported by extensive laboratory testing with good results for fatigue and roughness prediction [37, 38]. There is some concern
about the quality of the distress models, particularly for the asphalt longitudinal cracking model, as reported in Minnesota, South Carolina, and Oregon [39–41].

Although the MEPDG develops the whole idea of incremental design, it lacks simplicity, and maybe some models should be reviewed for the sake of applicability for road agencies and practitioners. The future research areas for MEPDG development and improvement are robust sensitivity analysis, enhancements of the climate model and the potential impact of climate change, traffic data quality control, local calibration, and new materials [42]. The published research about MEPDG is extensive and the authors of this review do not pretend to offer a comprehensive examination of every document, but to give an overview of the mainstream lines of work.

Despite the efforts invested in the MEPDG, there is not a consensus in the USA for its implementation. For example, the California Department of Transportation (Caltrans) developed the CalME software and postulates that “its models and ideas will become part of a multistate or national long-term research and development programs” [43]. The CalME software includes the entire range of design methods used in California, from the empirical procedure and a conventional mechanistic-empirical method, based on the Asphalt Institute design criteria, to a new recursive-incremental procedure, with emphasis on the design of overlays, based on the calibration of material properties from tests with heavy vehicle simulator (HVS). The recursive-incremental procedure predicts pavement conditions in terms of fatigue cracking, reflective cracking, rutting, and smoothness in increments of time using the output from one increment as input to the next increment. CalME evaluates the reliability of pavement distress through Monte Carlo simulation [44]. A similar improvement comes from the Texas Transportation Institute (TTI) with the development of the Texas mechanistic-empirical flexible pavement design system (TxME). The TxME software follows the incremental procedure of MEPDG and CalME but differs on the materials models for cracking in asphalt mixes, considering both crack initiation and propagation for fatigue and reflective cracking, and for rutting in asphalt mixes, granular layers and subgrade. The top-down cracking receives detailed consideration, as previously discussed in MEPDG research. As CalME, TxME improves the evaluation of the reliability of pavement distress through the Rosenblueth method, an alternative to Monte Carlo simulation [45].

**Perpetual pavement design**

The perpetual pavement design is a subset of mechanistic-empirical design with two main features: (1) it pursues to achieve a long life with no deep structural distress as bottom-up fatigue and rutting below the concrete layers, and (2) the method recognizes that all materials have endurance limits below which no damage will occur. Thus, the method seeks to avoid a terminal structural condition and the damage ratio \( D = \frac{N_{\text{expected}}}{N_{\text{allowable}}} \) must be lesser than 1.0. The pavements are expected to perform for 50 years or more without requiring major structural rehabilitation or reconstruction [46].

The typical section of a perpetual pavement consists of three hot-mix asphalt layers over a pavement foundation: the bottom layer is a fatigue-resistant material (rich in asphalt, low air-voids, 75-100 mm thick), the intermediate layer is a rut resistant material (high modulus, 100-175 mm thick), and the wearing surface is also rut resistant, but durable and impermeable [40-75 mm thick] [47]. The tensile strain fatigue endurance limit (FEL) of asphalt mixes varies between 60 to 200 \( \mu \varepsilon \) and is a function of the mix type [45]. The structural rutting is controlled by a vertical compressive strain in the subgrade of 200 \( \mu \varepsilon \) or a ratio between vertical stress and unconfined compressive strength lower than 0.42.

**4. Conclusions**

The authors presented a five-element geotechnical-based framework for the analysis of pavements. Among the elements in that framework, the Design of pavements comprises the definition of thicknesses, qualities, and construction specifications, and the calculation of budgets considering a user-defined level of reliability.

The design of asphalt pavements for roads and streets evolved from purely empirical to mechanistic-empirical procedures through the twentieth century. The mechanistic-empirical procedures also evolved from the determination of allowable load repetitions, based on asphalt fatigue and subgrade rutting, to incremental-recursive methods that simulate the development of primary distresses, like fatigue and permanent deformation in all layers, into functional distress expressed as roughness. More remarkable yet, design reliability is evolving from the single adjustments of the traffic intensity [AASHTO 1993] or the subgrade design-value [Asphalt Institute] to simulations based on the Monte Carlo (CalME) or Rosenblueth (TxME) methods.

Table 3 summarizes the characteristics of several empirical and M-E methods, providing an overview of the
Table 3 Empirical and M-E design procedures for asphalt pavements. Adapted from [14]

| Organization                                      | Pavement model | Modes of distress | Environmental effects | Pavement materials | Design format                  |
|---------------------------------------------------|----------------|-------------------|-----------------------|-------------------|-------------------------------|
| United States Army Corps of Engineers [8]         | SHS            | SSF               | M                     | HMA               | Design charts or equations    |
| American Association of State Highway and         | LES            | △PSI              | T [fix], M            | HMA               | AASHTO performance algorithm  |
| Transportation Officials [10]                     |                |                   |                       | UAg               |                               |
| Shell International Petroleum Company [27]        | LES            | FTL, SRC, ACR     | T                     | HMA               | Design charts BISAR program    |
| The Asphalt Institute, Lexington, KY, USA [MS-1,  | LES            | FTL, SR           | T, F                  | HMA               | SPDM 3.0 program              |
| MS-11, MS-23] [48]                                |                |                   |                       | ATM               |                               |
| Laboratoire Central des Ponts et Chaussés [29]    | LES            | FTL, SR           | T                     | HMA               | Design catalog ALIZE program  |
| National Institute for Transportation and Road    | LES            | FTL, SR, GBR      | T                     | HMA               | Design catalog PADS program   |
| research [NITRR], South Africa [49]               |                |                   |                       | CSAg              |                               |
| Austroads [50]                                    | LES            | FTL, SR           | T, M                  | HMA               | Design charts CIRCLY program  |
| National Cooperative Highway Research Program     | LES            | FTL, SR, ACH, LTC | T, M                  | HMA               | JULEA program                 |
| (NCHRP) Project 1-37A [AASHTO MEPDG] [25]        |                |                   |                       | UAg               |                               |
| California Department of Transportation CalME      | LES            |                   | T                     | HMA               | CalME program based on OpenPave|
| software [44]                                    |                |                   |                       | UAg               |                               |
| Texas Mechanistic-                                | LES            | FTL, ACH, SR, LTC | T, M                  | HMA               | TxME program based on WESLEA   |
| Empirical Pavement Design System [TxME] [45]      |                |                   |                       | UAg               |                               |

1. Pavement model: SHS: Solid half-space, LES: Layered elastic solid.
2. Modes of distress: SSF: Subgrade shear failure, △PSI: loss of serviceability, FTL: Fatigue in treated layers, SR: Vertical strain associated rutting in the subgrade, ACR: Asphalt concrete rutting, GBR: Untreated granular bases rutting, ACH: Asphalt concrete time hardening, LTC: Low-temperature cracking, RC: Reflective cracking.
3. Environmental effects: T: Temperature, M: Moisture, F: Soil freezing and thawing.
4. Pavement materials: HMA: Hot-mix asphalt or asphalt concrete, UAg: Untreated base aggregates, CSAg: Chemical-stabilized materials, ATM: Asphalt-treated materials.

The empirical method based on the CBR test is simple to use but limited by the bounds of the experimental data. Engineers should be aware of the simplifications that lead from the CBR curves in Figure 2 to extrapolations like Figure 3 based on successive transformations of the traffic categories from “typical” axle loads to traffic intensities (trucks per day) and, after the AASHO Road Test, to repetitions of the equivalent single axle load (ESAL) of 18...
kips [8].

The empirical character of the AASHTO method is troublesome for the present-day design given the limitations of factors as the structural and drainage coefficients, the ESAL equations, and the limited experience with thick asphalt layers and mix design [46]. More significant, the design criteria, based on the loss of_serviceability, is no longer measured nor calibrated, and its statistical relationship with modern-day experience with thick asphalt layers and mix design limitations of factors as the structural and drainage troublesomeness for the present-day design given the empirical character of the AASHTO method is appropriate without knowledge about the fundamental design factors and calibration of the performance models for each distress mode upon consideration. The highway agencies must be encouraged to invest in research and implementation to avoid undesirable practices like employing advanced M-E software with only a few CBR tests as primary information.

5. Declaration of competing interest

None declared under financial, professional, and personal competing interests.

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References

[1] A. Das, “Structural design of asphalt pavements: Principles and practices in various design guidelines,” Transportation in Developing Economies, vol. 1, July 21 2015. [Online]. Available: https://doi.org/10.1007/s40890-015-0004-3
[2] Z. Wu, G. Flintsch, A. Ferreira, and L. de Picado, “Framework for multiobjective optimization of physical highway assets investments,” Journal of Transportation Engineering, vol. 138, no. 12, May 29 2012. [Online]. Available: https://doi.org/10.1061/ASCETE.1943-5436.0000458
[3] E. J. Yoder and M. W. Witzczak, Principles of Pavement Design, 2nd ed. New York, USA: John Wiley & Sons, Inc., 1975.
[4] N. C. Yang, Design of Functional Pavements. New York, USA: McGraw-Hill, 1972.
[5] Y. H. Huang, Pavement Analysis and Design, 2nd ed. Upper Saddle River, NJ: Pearson Prentice Hall, 2004.
[6] R. B. Mallick and T. Eli-Kochi, Pavement Engineering: Principles and Practice, 1st ed. Boca Raton, Florida: CRC Press Taylor & Francis Group, 2009.
[7] C. R. Gonzales, W. R. Barker, and A. Bianchini, “Reformulation of the CBR procedure report i: Basic report,” U.S. Army Engineer Research and Development Center, Vicksburg, Mississippi, Tech. Rep. ERDC/GSL TR-12-16, Apr. 2012.
[8] G. W. Jameson, “Origins of AUSTRADS design procedures for granular pavements,” ARRB Transport Research Ltd, Vermont South, Australia, Tech. Rep. ARR 292, Sep. 1996.
[9] Pavement Design – A Guide to the Structural Design of Road Pavements, Austroads, Sydney, Australia, 1992.
[10] Guide for Design of Pavement Structures, AASHTO, Washington D.C., USA, 1993.
[11] L. H. Nguyen, “Research on the correlation between international roughness index (IRI) and present serviceability index (PSII), recommendations on evaluation rates in Vietnam's conditions,” International Journal of Engineering Research & Technology, vol. 13, no. 9, pp. 266–271, Sep. 2014.
[12] B. Al-Omari and M. Darter, “Relationships between international roughness index and present serviceability rating,” Transportation Research Record 1435, pp. 130–136, 1994.
[13] D. M. Burmister, “The theory of stresses and displacements in layered systems and application to design of airport runways,” in Proceeding HRB, Washington D.C., USA, 1943, pp. 126–148.
[14] C. L. Monismith, “Evolution of long-lasting asphalt pavement design. distinguished lecture international society for asphalt pavements,”
in International Symposium on Design and Construction of Long Lasting Asphalt Pavements, Auburn, Alabama, 2004.

[15] M. E. Harr and C. W. Lovell, "Vertical stresses under certain axisymmetric loadings," Highway Research Record, vol. 39, pp. 68–81, 1963.

[16] W. K. Kai, "Analysis and calculation of stresses and displacements in layered elastic systems," Acta Mechanica Sinica, vol. 3, pp. 251–260, Aug. 1987.

[17] J. W. Maina, Y. Ozawa, and K. Matsui, "Linear elastic analysis of pavement structure under non-circular loading," Road Materials and Pavement Design, vol. 13, no. 3, August 01 2012. [Online]. Available: https://doi.org/10.1080/14680629.2012.705419

[18] A. Louizi, L. Al-Qadi, and M. A. Elseifi, "Difference between in situ flexible pavement measured and calculated stresses and strains," Journal of Transportation Engineering, vol. 132, no. 7, July 2006. [Online]. Available: https://doi.org/10.1061/(ASCE)0733-947X(2006)132:7(574)

[19] A. T. Papagiannakis and E. A. Masad, Pavement Design and Materials, 1st ed. Hoboken, NJ: John Wiley & Sons, Inc., 2008.

[20] R. B. Freeman and M. E. Harr, "Stress predictions for flexible pavement systems," Journal of Transportation Engineering, vol. 130, no. 4, June 15 2004. [Online]. Available: https://doi.org/10.1061/(ASCE)0733-947X(2004)130:4(449)

[21] A. R. Ghanizadeh and M. R. Ahadi, "Application of artificial neural networks for analysis of flexible pavements under standard axle loading," International Journal of Transportation Engineering, vol. 3, no. 1, pp. 31–43, Jul. 2015.

[22] A. R. Ghanizadeh, "Application of support vector machine regression for predicting critical responses of flexible pavements," International Journal of Transportation Engineering, vol. 4, no. 4, pp. 305–315, Mar. 2017.

[23] Y. H. Cho, B. F. McCullough, and J. Weismann, "Considerations on finite-element method application in pavement structural analysis," Transportation Research Record: Journal of the Transportation Research Board, vol. 1539, no. 1, January 01 1996. [Online]. Available: https://doi.org/10.1177/0361198196153900113

[24] M. Y. Shahin, Pavement Management for Airports, Roads, and Parking Lots, 2nd ed. USA: Springer, 2006.

[25] Guide for Mechanistic-Empirical Design of New and Rehabilitated Pavement Structures, NCHRP, Washington D.C., USA, 2004.

[26] Overseas Road Note 19 A guide to the design of hot mix asphalt in tropical and sub-tropical countries, Transport Research Laboratory, Crowthorne, Berkshire, United Kingdom, 2002.

[27] Shell Pavement Design Software for Windows, Shell International Petroleum Company, London, 2000.

[28] J. F. Corté and M. T. Goux, "Design of pavements structures: The french technical guide," Transportation Research Record: Journal of the Transportation Research Board, vol. 1539, no. 1, January 01 1996. [Online]. Available: https://doi.org/10.1177/0361198196153900113

[29] Conception et dimensionnement des structures de chaussée, Laboratoire Central des Ponts et Chaussées, Paris, France, 1994.

[30] P. Pereira and J. Pais, "Main flexible pavement and mix design methods in europe and challenges for the development of an european method," Journal of Traffic and Transportation Engineering, vol. 4, no. 4, August 2017. [Online]. Available: https://doi.org/10.1016/j.jtte.2017.06.001

[31] T. Ingason and et al., "Amadeus - advanced models for analytical design of european pavement structures," Tech. Rep. RO-97-SC.2137, Jan. 2000.

[32] C. W. Schwartz and R. L. Carvalho, "Implementation of the NCHRP 1-37A design guide," University of Maryland, Maryland, USA, Tech. Rep., 2007.

[33] AASHTO, Mechanistic-empirical Pavement Design Guide: A Manual of Practice. Washington D.C., USA: American Association of State Highway and Transportation Officials, 2008.

[34] L. M. Pierce and C. McGovern, "Implementation of the AASHTO mechanistic-empirical pavement design guide and software," Transportation Research Board, Washington D.C., USA, Tech. Rep. NCHRP Synthesis 457, 2014.

[35] N. Tran, M. M. Robbins, C. Rodezno, and D. H. Timm, "Pavement ME design - impact of local calibration, foundation support, and design and reliability thresholds," National Center for Asphalt Technology, Auburn, Alabama, Tech. Rep. NCAT Report 17-08, Sep. 2017.

[36] C. W. Schwartz, S. H. Kim, H. Ceylan, K. Gopalakrishnan, and R. Li, "Sensitivity evaluation of MEPDG performance prediction," Iowa State University, Maryland, USA, Tech. Rep. NCHRP Project 1–47, 2011.

[37] T. Kasperick and K. Ksabaiti, "Calibration of the mechanistic-empirical pavement design guide for local paved roads in Wyoming," The Mountain Plains Consortium, Laramie, Wyoming, Tech. Rep. MPC 15-294, Dec. 2015.

[38] Y. R. Kim, F. M. Jadoun, T. Hou, and N. Muthadi, "Local calibration of the MEPDG for flexible pavement design," North Carolina Department of Transportation, Raleigh, NC, Tech. Rep. FHWA-NC-2007-07, Oct. 2011.

[39] R. Velasquez and et al., "Implementation of the MEPDG for new and rehabilitated pavement structures for design of concrete and asphalt pavements in Minnesota," Minnesota Department of Transportation, Saint Paul, Minnesota, Tech. Rep. MnDOT 2009–06, 2009.

[40] R. L. Bausand N. R. Stires, "Mechanistic-empirical pavement design guide implementation," Department of Civil and Environmental Engineering - The University of South Carolina, Columbia, South Carolina, Tech. Rep. FHWA-SC-10-01, Jun. 2010.

[41] R. C. Williams and R. Shaidur, "Mechanistic-empirical pavement design guide calibration for pavement rehabilitation," Oregon Department of Transportation - Federal Highway Administration, Salem, Oregon, Tech. Rep. SPR 718, 2013.

[42] Q. Li, D. X. Xiao, K. C. P. Wang, K. D. Hall, and Y. Qiu, "Mechanistic-empirical pavement design guide (MEPDG): A bird’s-eye view," Journal of Modern Transportation, vol. 19, no. 2, June 2013. [Online]. Available: https://doi.org/10.1007/BF03325749

[43] P. Ullitd and et al., "CalME, a mechanistic-empirical program to analyze and design flexible pavement rehabilitation," Transportation Research Record: Journal of the Transportation Research Board, vol. 2153, November 2010. [Online]. Available: https://doi.org/10.3141/2153-16

[44] (2019) Calme version 3 help file. University of California Pavement Research Center UCPRC. Accessed Jan. 31, 2020. [Online]. Available: https://bit.ly/2Jp6vNj

[45] S. Hu, F. Zhou, and T. Scullion, "Texas M-E flexible pavement design system: Literature review and proposed framework," Texas Department of Transportation Research and Technology Implementation Office, Austin, Texas, Tech. Rep. FHWA-TX-12-0-6622-1, Apr. 2012.

[46] D. H. Timm, M. M. Robbins, N. Tran, and C. Rodezno, "Flexible pavement design - state of the practice," National Center for Asphalt Technology, Auburn, AL, Tech. Rep. NCAT Report 14/04, Aug. 2014.

[47] D. E. Newcomb, M. Buncher, and I. J. Huddleston, "Concepts of perpetual pavements," Transportation Research Board, vol. 503, pp. 4–11, 2001.

[48] A. Institute, Thickness Design: Asphalt Pavements for Highways & Streets. Lexington, Kentucky: Asphalt Institute, 1981.

[49] R. N. Walker, W. D. O. Patterson, C. R. Freeme, and C. P. Marias, "The south african mechanistic pavement design procedure," in 4th International Conference on the Structural Design of Asphalt Pavements, Lino Lakes, Minnesota, 1977.

[50] Pavement Design - A Guide to the Structural Design of Road Pavements. Interim Version of Revised Overlay Design Procedures, Austroads, Sydney, Australia, 1994.