The California-Kepler Survey. X. The Radius Gap as a Function of Stellar Mass, Metallicity, and Age

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Abstract

In 2017, the California-Kepler Survey (CKS) published its first data release (DR1) of high-resolution optical spectra of 1305 planet hosts. Refined CKS planet radii revealed that small planets are bifurcated into two distinct populations, super-Earths (smaller than 1.5 \( R_{\oplus} \)) and sub-Neptunes (between 2.0 and 4.0 \( R_{\oplus} \)), with few planets in between (the “radius gap”). Several theoretical models of the radius gap predict variation with stellar mass, but testing these predictions is challenging with CKS DR1 due to its limited \( M_* \) range of 0.8–1.4 \( M_\odot \). Here we present CKS DR2 with 411 additional spectra and derived properties focusing on stars of 0.5–0.8 \( M_\odot \). We found that the radius gap follows \( R_p \propto P^{\alpha} \) with \( m = -0.10 \pm 0.03 \), consistent with predictions of X-ray and ultraviolet- and core-powered mass-loss mechanisms. We found no evidence that \( m \) varies with \( M_* \). We observed a correlation between the average sub-Neptune size and \( M_* \). Over 0.5–1.4 \( M_\odot \), the average sub-Neptune grows from 2.1 to 2.6 \( R_{\oplus} \), following \( R_p \propto M_*^{\alpha} \) with \( \alpha = 0.25 \pm 0.03 \). In contrast, there is no detectable change for super-Earths. These \( M_* - R_p \) trends suggest that protoplanetary disks can efficiently produce cores up to a threshold mass of \( M_* \), which grows linearly with stellar mass according to \( M_* \approx 10 M_{\oplus} (M_*/M_\odot) \). There is no significant correlation between sub-Neptune size and stellar metallicity (over −0.5 to +0.5 dex), suggesting a weak relationship between planet envelope opacity and stellar metallicity. Finally, there is no significant variation in sub-Neptune size with stellar age (over 1–10 Gyr), which suggests that the majority of envelope contraction concludes after \( \sim 1 \) Gyr.

Unified Astronomy Thesaurus concepts: Exoplanet astronomy (486); Exoplanet formation (492); Transit photometry (1709); Exoplanets (498); Super Earths (1655); Mini Neptunes (1063); High resolution spectroscopy (2096)

Supporting material: machine-readable tables

1. Introduction

The key legacy of NASA’s Kepler mission is its sample of over 4000 extrasolar planets. These planets were discovered from precise, nearly continuous photometry obtained over 4 yr of roughly 200,000 stars. Importantly, the Kepler planet population covers a wide range of sizes and orbital periods; sizes range from super-Jupiter to sub-Mercury, and orbital periods extend from less than a day to more than a year (Thompson et al. 2018). The Kepler exoplanet census has, and orbital migration. Gaining insights into these processes requires detailed knowledge of host stars. Until 2017, the properties of the vast majority of Kepler planet host stars were based on broadband photometry, which limited the accuracy of star and planet properties. Importantly, photometric stellar radii \( R_* \) were uncertain at the \( \sim 40\% \) level (Brown et al. 2011).

To address these limitations, our group conducted the California-Kepler Survey (CKS; Petigura et al. 2017), a spectroscopic survey of 1305 planet-hosting stars observed by Kepler (technically Kepler Objects of Interest, or KOIs). The CKS consisted of several overlapping samples, the largest of which was magnitude-limited and included 960 planet hosts brighter than Kepler-band magnitude \( m_{Kep} = 14.2 \). Using these spectra, we measured \( T_{\text{eff}}, \log g, \) and [Fe/H] and refined stellar \( M_* \), \( R_* \), and age, along with planet size \( R_p \) and incident stellar flux \( S_{\text{Inc}} \).

The CKS stellar properties enabled several insights into the occurrence and properties of planets as a function of stellar metallicity (Petigura et al. 2018b), stellar age (Berger et al. 2018a),...
planet multiplicity (Weiss et al. 2018), stellar obliquity (Winn et al. 2017), and other properties. One such insight flowed directly from the improvement in $R_e$ errors from 40% to 10%; the radius distribution of small planets is bimodal (Fulton et al. 2017). This result has been confirmed in samples of planets with even smaller radius uncertainties that have leveraged asteroseismic or parallax constraints (Berger et al. 2018b; Fulton & Petigura 2018; Van Eylen et al. 2018; Petigura 2020).

This radius gap was predicted by several groups who considered the effect of photoevaporation on planetary envelopes by X-ray and extreme-ultraviolet (XUV) radiation (Lopez & Fortney 2013; Owen & Wu 2013; Jin et al. 2014; Chen & Rogers 2016). Other processes that inject energy into planet envelopes may also produce the gap, such as the luminosity from cooling cores (Ginzburg et al. 2018; Gupta & Schlichting 2019) or the heat from accreting planetesimals (Chatterjee & Chen 2018; Zeng et al. 2019; Wyatt et al. 2020).

Projecting the planet population along the axis of stellar mass should help illuminate which processes sculpt the distribution of small planets. For example, photoevaporation models predict that small planets will lose their envelopes out to lower bolometric flux levels around low-mass stars due to increased $F_{\text{XUV}}/F_{\text{bol}}$.

Such studies are challenging with CKS DR1 because it spans a limited range of $M_* \approx 0.8–1.4 M_\odot$. There are several reasons for this: (1) the Kepler selection function favored FGK stars (Batalha et al. 2010), (2) most of the Kepler stars below 0.8 $M_\odot$ are fainter than $m_{\text{Kep}} = 14.2$, and (3) the spectroscopic techniques used in Petigura et al. (2017) could not return reliable parameters for stars cooler than $T_{\text{eff}} = 4700$ K. Despite the limited $M_*$ range, analyses of this data set indicated an increase in the average size of sub-Neptunes with increasing stellar mass (Fulton & Petigura 2018; Petigura 2020). In addition, Wu (2019) and Berger et al. (2020b) found a positive $M_*–R_p$ correlation for sub-Neptunes.

The $T_{\text{eff}} > 4700$ K boundary in CKS poses an additional challenge for interpreting trends with $M_*$. This boundary corresponds to $M_* > 0.65$ and 0.80 $M_\odot$ at [Fe/H] = −0.4 and +0.4 dex, respectively, the upper and lower ends of the CKS metallicity distribution. Owen & Murray-Clay (2018) discussed how this correlation acts as a confounding factor for interpreting both mass and metallicity trends in CKS DR1.

Here we present a follow-up survey designed to expand the stellar-mass range of the CKS sample. We constructed a sample of planet hosts spanning 0.5–1.4 $M_\odot$ (Section 2) and gathered Keck/HIRES spectra of those absent from CKS DR1. New spectra of 411 hosts are presented here as CKS DR2 (Section 3). We analyzed the combined DR1/DR2 samples to derive temperatures, metallicities, and limits on stellar companions, which we combined with astrometric and photometric measurements to derive stellar masses, radii, and ages (Section 4). With updated stellar properties, we refined the precision and purity of the planet catalog (Section 5). We analyzed both the distribution of detected planets (Section 6) and the underlying occurrence rate (Section 7). We offer some comparisons to planet formation theory (Section 8) and provide a brief summary and conclusion (Section 9).

2. Sample Selection

Our main goal was to measure planet occurrence as a function of stellar mass. This requires a sample of planets drawn from a well-defined sample of stars spanning a broad range in stellar mass. Before describing our selection function in detail, we first orient the reader with an overview of our survey design and practical considerations. When we designed our survey in 2018, our goal was to increase the number of low-mass stars with CKS-quality parameters given a fixed telescope allocation of 15 Keck/HIRES nights. Simply extending the magnitude-limited survey beyond $m_{\text{Kep}} = 14.2$ would have included many stars with $T_{\text{eff}} \approx 5000–6500$ K that were already well-sampled by DR1 (see Figure 1). Observing all targets down to $m_{\text{Kep}} = 16.0$ in the manner described in Section 3 would have required ~75 nights and was impractical. Instead, we adopted a selection function and observing strategy that favored cool stars but mitigated magnitude-dependent effects. The two mitigation strategies are described in detail in Sections 2–5 but briefly involved selecting single isolated stars and collecting spectra of homogeneous quality.

We began with 184,933 stars in the union of the following three catalogs: the Kepler project Data Release 25 (DR25) stellar properties catalog (Mathur et al. 2017, hereafter M17), the Gaia DR2 catalogue (Gaia Collaboration et al. 2018), and the Berger et al. (2020b, hereafter B20) catalogue of stellar properties. We then applied the following filters.

1. Stellar brightness and effective temperature. Our sample consists of two magnitude-limited components. If $T_{\text{eff}} = 5000–6500$ K (as measured by M17), we required $m_{\text{Kep}} < 14.2$; if $T_{\text{eff}} = 3000–5000$ K, we required $m_{\text{Kep}} < 16.0$. A total of 77,243 stars remained.

2. Main-sequence stars. We selected main-sequence stars using their position in the Gaia color–magnitude diagram. Stars were included if they reside within the boundaries shown in Figure 1. A total of 47,502 stars remained.

3. Single stars: Gaia source catalog. If a transit is observed within a Kepler aperture containing more than one star, it is often not possible to identify the star hosting the transiting object. Whichever star is the host, the transit depth is diluted by the neighboring star(s), and the inferred planet radius will be biased to smaller values. To ensure high-precision $R_p$, we worked to exclude targets that are diluted by >10%, which would result in an $R_p$ error of >5%. We excluded stars where the cumulative G-band flux contribution from all Gaia-identified neighboring stars within 4º exceeded 10%. Companions outside of this limit are resolved as separate sources in the KIC, which had an average FWHM of 2.5″ (Brown et al. 2011). The Kepler project removed the diluting flux from such sources during the photometric extraction (see the discussion of the “crowding metric” in Stumpe et al. 2012). A total of 46,468 stars remained.

4. Single stars: Gaia astrometric noise. Companions within 1″ are often not released as separate sources in Gaia DR2 but can be identified using the residuals to the astrometric fits. The Gaia renormalized unit weight error (RUWE) is conceptually similar to the square root of the reduced $\chi^2$ and close to unity when the astrometric data are consistent with parallax and proper motion only, with no additional variation due to any companions (Lindegren 2018). Analyses of stars with high-resolution imaging have demonstrated that requiring RUWE < 1.2 removes companions with $\Delta m_2 < 3$ mag and separations of $\rho = 0″1–1″$ (Bryson et al. 2020; Wood et al. 2021; A. L. Kraus et al. 2022, in preparation). A total of 39,423 stars remained.
We cross-referenced these stars against the Thompson et al. (2018, hereafter T18) catalog of KOIs, which we accessed from the NASA Exoplanet Archive (NEA; Akeson et al. 2013). This catalog was derived from the final planet search conducted by the Kepler project (DR25). Among our filtered stellar sample, T18 lists 39,423 stars hosting 2373 KOIs. We subjected the KOIs to the following additional filters.

5. Candidate reliability. T18 dispositioned KOIs using a fully automated procedure called the Robovetter that performed a series of tests on a suite of data quality metrics designed to identify false positives due to data anomalies and eclipsing binaries. When setting the Robovetter thresholds, T18 emulated the human classification of the Threshold Crossing Event Review Team. Robovetter dispositioned all KOIs as either “false positive” or “planet candidate.” Some KOIs fall near the boundary between the two dispositions. Through Monte Carlo simulations, T18 quantified the proximity of each KOI to this boundary. They reported a “disposition score,” which is the fraction of Monte Carlo simulations classified as planet candidates. We required “planet candidate” status13 with a disposition score14 exceeding 75%. Finally, we removed a handful of known false 

 positives that cleared the Robovetter that are listed in the DR25 supplemental table.15 A total of 1425 KOIs orbiting 1003 host stars remained.

6. Candidate signal-to-noise ratio (S/N). Low-S/N candidates are more likely to be false positives (see, e.g., Bryson et al. 2020) and yield lower overall precision on Rp/Rs. The Kepler project reported S/N as a “multiple event statistic” (MES; Jenkins 2002).16 We required MES > 10. A total of 1250 KOIs orbiting 891 host stars remained.

7. Transit modeling. To compute planet properties, we used posterior samples of transit parameters derived from Markov Chain Monte Carlo (MCMC). As a small fraction of the T18 KOIs were not modeled using MCMC,17 most of these are dispositioned as false positives. We removed a handful of candidates that passed the previous cuts. A total of 1246 KOIs orbiting 888 host stars remained.

Figure 1 shows the application of these filters to the field star and planet samples. In this paper, we refer to these 888 stars as the “CKS extended mass” (CXM) sample.

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13 NEA data column: koi_pdisposition.
14 NEA data column: koi_score.
15 NEA data column: koi_pdisposition.
16 NEA data column: koi_max_mult_ev.
17 NEA data column: koi_fittype.
3. Spectroscopic Observations

We worked to compile a homogeneous spectroscopic catalog of all CXM stars from new and archival observations. All spectra were obtained with Keck/HIRES (Vogt et al. 1994) to ensure common systematics in our analysis. Our goal was to gather spectra with $R \geq 60,000$ and $S/N \geq 20$ pixel$^{-1}$ on blaze at 5500 Å.

The inventory of DR1/DR2 spectra and the CXM host star sample are shown in Figure 2. By design, there was substantial overlap between the 1305-star DR1 sample and the CXM sample (628/888 spectra). The DR1 spectra have $R \geq 60,000$ and $S/N \geq 45$ pixel$^{-1}$ and thus met our spectral quality goals. The 411 spectra in DR2 are a mixture of 81 archival HIRES spectra taken before 2018 and 330 new spectra taken by our team since then. For the archival spectra, all have $R \geq 60,000$, and all but four had $S/N \geq 20$ pixel$^{-1}$. An additional 260/888 CXM stars have spectra in DR2.

Below, we describe the observations of the post-2018 DR2 spectra, which were executed as part of a NASA Key Strategic Mission Support program (PI: Petigura). Our strategy was identical to that of CKS DR1, except we exposed to a lower S/N. We used the standard setup of the California Planet Search (CPS; Howard et al. 2010). We observed stars through the “C2” slit with sky-projected dimensions of 0"86 × 14"0, which achieves a spectral resolution of $R \approx 60,000$. We used the exposure meter to attain a designed S/N, which is measured at the peak of the blaze function at $\lambda = 5500$ Å.

Given the magnitude-limited nature of DR1, most DR2 stars had $m_{Kep} = 14.2$–16.0 mag. It would have been prohibitively expensive to observe these stars to the same $S/N$ level as DR1 (45 pixel$^{-1}$), so we used the exposure meter to achieve $S/N = 20$ pixel$^{-1}$ for stars in this magnitude range. In Section 4, we demonstrate that the additional photon-limited uncertainties are smaller than other sources of uncertainty in the extracted parameters.

For faint targets, the sky background is occasionally comparable to the stellar spectrum, depending on moon separation, moon phase, and cloud cover. In our spectral reduction, we removed the sky background (see Batalha et al. 2011 for details), but it still contributes to exposure meter counts. Thus, at a fixed $m_V$ and exposure meter setting, additional sky background would cause exposures to terminate early. While at the telescope, we used a custom script to compute the sky contribution in real time and adjusted the exposure meter setting such that we would reach the desired S/N after sky subtraction.

We reduced our spectra according to the standard practices of CPS. We removed the blaze function by dividing our spectra by a composite spectrum of spectrally flat standards compiled by Clubb et al. (2018). One component of our spectroscopic analysis involved registering each spectrum to a common wavelength scale. We used the SpecMatch-Empirical code (Yee et al. 2017), which includes a ladder of reference spectra that have been registered against the National Solar Observatory solar atlas (Kurucz et al. 1984). Figure 3 shows the Mg i b region for representative spectra over a range of $T_{\text{eff}}$. The deblazed spectra are available via the Keck Observatory Archive, the CFOP website, and a website maintained by our team. We have also made available the standard observatory-frame wavelength solution applicable to every spectrum, which is accurate to within 1 reduced pixel or 1.2 km s$^{-1}$. The registered spectra are also available at the above repositories.

4. Host Star Characterization

4.1. Spectroscopy

We derived stellar parameters from our spectra using two related and complementary codes: SpecMatch-Synthetic and SpecMatch-Empirical. Both codes were designed to yield high-quality parameters even at moderate or low S/N. A detailed description of SpecMatch-Synthetic is available in Petigura (2015), and the code’s application to CKS DR1 is given in Petigura et al. (2017). In brief, the code generates a synthetic spectrum by interpolating within a set of library spectra computed over a grid of $T_{\text{eff}}$, $\log g$, and [Fe/H]. It then applies line-broadening kernels that account for the instrumental profile, stellar rotation, and macroturbulence. The library spectra were computed by Coelho et al. (2005) under the assumption of local thermodynamic equilibrium (LTE) using the Castelli & Kurucz (2003) model atmospheres. The code derives $T_{\text{eff}}$, $\log g$, [Fe/H], and $v \sin i$ using nonlinear optimization of an $l_2$ metric, which is evaluated over five spectral segments with a combined spectral bandwidth of 380 Å between 5200 and 6260 Å.

The uncertainties of the SpecMatch-Synthetic parameters have been extensively vetted for stars having $T_{\text{eff}} = 4700$–6500 K. Errors are dominated by systematic uncertainties, which are $\sigma(T_{\text{eff}}) = 100$ K, $\sigma(\log g) = 0.10$ dex, and $\sigma([\text{Fe/H}]) = 0.06$ dex. Poisson uncertainties are smaller than systematic uncertainties even at low S/N because the code fits a wide spectral bandpass and combines information from many lines. At our lowest S/N (20 pixel$^{-1}$), photon-limited errors are $\sigma(T_{\text{eff}}) = 34$ K, $\sigma(\log g) = 0.05$ dex, and $\sigma([\text{Fe/H}]) = 0.02$ dex, respectively, below the systematic floor. Above 6500 K, the quality of the derived parameters degrades due to the reduced number of lines and substantial rotational broadening. As $T_{\text{eff}}$ drops below 4700 K, the number of lines in SpecMatch-Synthetic wavelength regions increases dramatically due to molecular features (of which MgH is the most prominent).

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18 http://www2.keck.hawaii.edu/koa/public/koa.php
19 http://cfop.ipac.caltech.edu
20 http://astro.caltech.edu/~howard/cks/
Table 1

Stellar Properties

| KOI | mK (mag) | π (mas) | Teff (K) | [Fe/H] | v sin i (km s⁻¹) | Prov | Rₜ (R☉) | Mₜ,iso (M☉) | Rₜ,iso (R☉) | ρₜ,iso (g cm⁻³) | age,iso (Gyr) | πspec (mas) | SB2 | CXM |
|-----|----------|--------|----------|--------|----------------|------|----------|-------------|-------------|----------------|---------------|-------------|-----|-----|
| 1   | 9.85     | 4.67   | 5857     | 0.02   | 1.3 syn        | 1.04 | 1.02    | 1.03        | 0.91        | 3.7            | 1.4           | 3.26        | 1   | 1   |
| 2   | 9.33     | 2.96   | 6403     | 0.22   | 5.1 syn        | 2.00 | 1.50    | 1.99        | 0.19        | 1.8            | 3.7           | 2.00        | 1   | 1   |
| 3   | 7.01     | 26.50  | 4619     | 0.16   | ... emp       | 0.78 | 0.76    | 0.75        | 1.79        | 11.2           | 23.80         | 1.99        | 1   | 1   |
| 4   | 10.20    | 1.29   | 5948     | −0.27  | 38.0 syn       | 3.26 | 1.45    | 3.22        | 0.04        | 2.0            | 0.93          | 2.00        | 3   | 0   |
| 6   | 10.99    | 2.13   | 6356     | 0.05   | 11.8 syn       | 1.29 | 1.23    | 1.28        | 0.57        | 1.5            | 2.24          | 1.99        | 1   | 1   |

Note. Properties of 1716 planet-hosting stars from the union of the DR1 and DR2 data sets. Here mK is the 2MASS K-band apparent magnitude, and π is the Gaia DR2 parallax. The Teff, [Fe/H], and v sin i were derived by one of two methods listed in the “Prov” column: “syn,” SpecMatch-Synthetic, and “emp.” SpecMatch-Empirical. Here Rₜ is our adopted stellar radius from the Stefan-Boltzmann law. Stellar properties with the “iso” subscript incorporate constraints from the MIST isochrones. Here “SB2” encodes the limits on spectroscopic binaries (SB2s) using the ReaMatch code (Kobal et al. 2015): 1, no detection of SB2 with ΔmV ≤ 5 mag and ΔRV ≥ 12 km s⁻¹; 2, Teff < 3500 K, star unfit for ReaMatch; 3, v sin i > 10 km s⁻¹, star unfit for ReaMatch; 4, ambiguous detection; 5, obvious detection. Note: ReaMatch computes Teff and v sin i independently from SpecMatch-Synthetic and SpecMatch-Empirical. The “CXM” flag is 1 if the star is in the 888-star CXM subset. Median uncertainties are as follows: mK, 0.02 mag; π, 1.4%; Teff, 100 K; [Fe/H], 0.06 dex; v sin i, 1 km s⁻¹; Rₜ, 3.9%; Mₜ,iso, 3.7%; Rₜ,iso, 2.6%; ρₜ,iso, 8.9%; age,iso, 0.24 dex; πspec, 16%. (This table is available in its entirety in machine-readable form.)
4.2. Stellar Properties

We derived stellar masses, radii, and ages using our spectroscopic measurements of $T_{\text{eff}}$ and [Fe/H], along with astrometric and photometric constraints. Our methodology closely follows that of Fulton & Petigura (2018). We give a brief summary below, noting differences where relevant.

We measured $R_*$ using the isoclassify package in its “direct” mode. This code evaluates $R_*$ from the Stefan–Boltzmann law,

$$ R_* = \left( \frac{L_{\text{bol}}}{4 \pi \sigma_b T_{\text{eff}}^4} \right)^{1/2}, \quad (1) $$

where $L_{\text{bol}}$ is the bolometric stellar luminosity, and $\sigma_b$ is the Stefan–Boltzmann constant. Here $L_{\text{bol}}$ is directly related to bolometric magnitude $M_{\text{bol}}$, which may be expressed as

$$ M_{\text{bol}} = m - \mu - A + BC, \quad (2) $$

where $m$ is the apparent magnitude, $\mu$ is the distance modulus, $A$ is the line-of-sight extinction, and $BC$ is the bolometric correction. We summarize each input below, along with their typical uncertainties. Given the discontinuity in our sample selection at $m_{\text{Kep}} = 14.2$ described in Section 2, we report median uncertainties above and below this value.

1. Apparent magnitude. We used Two Micron All Sky Survey (2MASS) K-band photometric measurements because dust extinction is less severe in the infrared. We used 2MASS $m_K$, which has a median precision of 0.02 mag for $m_{\text{Kep}} < 14.2$ and 0.03 mag for $m_{\text{Kep}} > 14.2$.

2. Extinction. We accounted for K-band extinction $A$ using the 3D dust map of Green et al. (2019), an update to the Green et al. (2018) map used in Fulton & Petigura (2018). Median $A$ is 0.01 mag for both bright and faint subsets.

3. Distance modulus. We used Gaia DR2 parallaxes and applied a correction of +0.053 mas to account for a known systematic offset in the Kepler field (Zinn et al. 2019). The parallaxes have a median precision of 1.2% for $m_{\text{Kep}} < 14.2$ and 1.8% for $m_{\text{Kep}} > 14.2$. Isoclassify handles the conversion between parallax and distance modulus using a Bayesian framework.

4. Bolometric correction. Isoclassify interpolates over a grid of bolometric corrections computed by the MESA Isochrones and Stellar Tracks project (MIST v1.2; Paxton et al. 2011, 2013, 2015; Choi et al. 2016; Dotter 2016). Uncertainties in $T_{\text{eff}}$ dominate the uncertainty of the K-band bolometric correction, and a 60 K uncertainty translates to an $\approx 0.03$ mag error on BC.

Table 1 lists our measured $R_*$, and Figure 4 shows the distribution of fractional $R_*$ uncertainties. The median fractional uncertainty is 4.0% for $m_{\text{Kep}} < 14.2$ and 4.4% for $m_{\text{Kep}} > 14.2$.

We also ran isoclassify in its “grid” mode with the same constraints. In this mode, the code queries the MIST isochrones, which provide various stellar properties over a grid of $M_*$, [Fe/H], and age. The grid extends to 20 Gyr to minimize grid edge effects, which can bias the parameter posteriors. At each grid point, isoclassify computes the likelihood that the point is consistent with the input constraints.

Marginalized values are determined by direct integration. We list $M_{*,\text{iso}}, R_{*,\text{iso}}, \rho_{*,\text{iso}}$, and $\text{age}_{*,\text{iso}}$ in Table 1. The “iso” subscript indicates that these parameters are forced to be consistent with MIST isochrones. The median fractional uncertainty for $M_{*,\text{iso}}$ is 3.8% for $m_{\text{Kep}} < 14.2$ and 3.7% for $m_{\text{Kep}} > 14.2$; for $\rho_{*,\text{iso}}$, it is 8.7% for $m_{\text{Kep}} < 14.2$ and 3.8% for $m_{\text{Kep}} > 14.2$. A handful of stars have age $\text{age}_{*,\text{iso}} > 14$ Gyr because the grid extends to 20 Gyr for the reasons explained above. Age uncertainties vary widely across the H-R diagram and are discussed in Section 6.

5. Planet Catalog

In the previous section, we computed stellar properties in the combined DR1/DR2 data set. For the remainder of the paper, we focus on the 1246 planets associated with the 888-star CXM subsample (see Figure 2). In this section, we first compute the planet properties given our updated stellar properties and then apply an additional set of quality checks to produce a high-reliability sample of planets for demographic work in later sections.

5.1. Planet Properties

We computed $R_p$ from our $R_*$ (listed in Table 1) and T18’s modeling of Kepler light curves. We multiplied our posterior samples on $R_*$ by the MCMC-derived posterior samples on $R_p/R_*$ (available at the NEA). The median fractional error on $R_p/R_*$ is 3.9% for $m_{\text{Kep}} < 14.2$ and 4.8% for $m_{\text{Kep}} > 14.2$. Uncertainties in $R_*$ and $R_p/R_*$ are independent and propagated into $R_p$, and we quote the 16th, 50th, and 84th posterior quantiles in Table 2. The median fractional precision in $R_p$ is 5.6% for $m_{\text{Kep}} < 14.2$ and 6.3% for $m_{\text{Kep}} > 14.2$. Figure 4 shows the fractional precision of $R_p, R_*$, and $R_p/R_*$ for most of the sample. $R_*$ errors are comparable to or larger than $R_p/R_*$ errors. However, for a small subset, $R_p/R_*$ errors dominate.

A note about the provenance of $R_p/R_*$: there are a number of published catalogs of $R_p/R_*$ from the Kepler project, of which T18 is the most recent. The NEA table corresponding to the T18 catalog lists the “best-fit” $R_p/R_*$, not the posterior medians. Petigura (2020) found that these best-fit values contribute noise to $R_p/R_*$ from the nonlinear optimization and recommended using posterior medians, which are a more robust estimator.

We compared our planet radii to T18 by computing the ratio of the radii, $r = R_{p,\text{iso}}/R_{p,T18}$. There was a negligible systematic offset mean($r$) = 1.00 but a substantial dispersion rms...
(r) = 20%. The dispersion is dominated by uncertainties in the T18 Rp.

Two additional quantities were relevant to our goal of precise planet radii: the observed transit duration T, and the expected duration of a centrally transiting planet on a circular orbit Tmax,circ. Here T refers to the time between the midpoints of first/second contact and third/fourth contact. In the T18 modeling, the transit shape was set by the following free parameters: period P, transit epoch T0, impact parameter b, mean stellar density assuming a circular orbit ρs,circ, and Rp/Rs. We derived T and its uncertainties according to

\[ T = 2.036 \text{ hr} (1-b^2)^{1/2} \left( \frac{P}{1 \text{ day}} \right)^{1/3} \left( \frac{\rho_{s,circ}}{1 \text{ g cm}^{-3}} \right)^{-1/3} \]  

using the T18 MCMC chains. We computed Tmax,circ according to

\[ T_{\text{max,circ}} = 2.036 \text{ hr} \left( \frac{P}{1 \text{ day}} \right)^{1/3} \left( \frac{\rho_{s,\text{inst}}}{1 \text{ g cm}^{-3}} \right)^{-1/3} . \]

Both T and Tmax,circ are listed in Table 2, along with semimajor axis a and incident stellar flux Sinc.

5.2. Refining the Planet Sample

While the initial CXM sample was optimized for high-reliability planets (Section 2), we incorporated additional diagnostics from our spectra to further increase sample purity. We first filtered on the following stellar properties.

1. Rotation rate. Our spectroscopic codes are unreliable at \( v \sin i > 20 \text{ km s}^{-1} \) (Petigura et al. 2017). We excluded 17 stars above this threshold that all had \( T_{\text{eff}} > 6500 \text{ K} \) as measured by B20. A total of 1227 KOIs orbiting 871 hosts remained.

2. Spectroscopic parallax. Following Fulton & Petigura (2018), we used isoclassify to compute a “spectroscopic parallax” constrained by our Teff, [Fe/H], mK, and the MIST models. If the spectroscopic and trigonometric parallaxes differ significantly, we conclude that the input parameters used to compute Rs are inconsistent due to unresolved binaries or other effects. We removed nine stars where these parallaxes differed by 4σ or more. We chose a 4σ over a 3σ threshold because the probability of a 3σ event is \( 3 \times 10^{-3} \); thus, we expect \( \approx \)three such events in a sample of \( \approx 10^5 \) stars. The probability of a 4σ event is \( 6 \times 10^{-5} \), so a single such event is unlikely. A total of 1215 KOIs orbiting 862 hosts remained.

3. Secondary spectra. We removed one star where we identified a secondary set of spectral lines using the methodology of Kolbl et al. (2015), which is sensitive to binaries having \( \Delta m_V \gtrsim 5 \text{ mag} \) and \( \Delta v > 12 \text{ km s}^{-1} \). A total of 1214 KOIs orbiting 861 hosts remained.

Next, we filtered based on the following planet properties.

14. Impact parameter. We removed grazing and high impact parameter planets by excluding planets where the median of the b posterior exceeded 0.8. Petigura (2020) found, however, that for most Kepler light curves, this cut is ineffective at excluding high-b transits because b is nearly unconstrained. For such transits, Rp/Rs is biased by 10%-20% due to the strong \( b-R_p/R_s \) covariance. However, \( T/T_{\text{max,circ}} \) is an effective proxy for b. In addition to our explicit filter on b, we also required \( T/T_{\text{max,circ}} > 0.6 \) in order to exclude transits with b > 0.8. While planets with eccentric orbits that transit near periastron also produce low \( T/T_{\text{max,circ}} \), Petigura (2020) showed that fewer than 20% of Kepler planets with \( T/T_{\text{max,circ}} < 0.6 \) have b < 0.8. A total of 973 KOIs orbiting 704 hosts remained.

15. Radius precision. We required fractional errors on Rp of 20% or less. A total of 970 KOIs orbiting 703 hosts remained.

The properties of the stars that passed these cuts are shown in Figure 5. They span a mass range of \( M \approx 0.5-1.4 M_{\odot} \).

6. Distribution of Detected Planets

From here on, we describe and interpret the features in our curated sample of 970 planets. In this section, we treat the population of detected planets before turning to the occurrence distribution in Section 7. We explore how the radius gap correlates with \( P, S_{\text{inc}}, M_s, \) and age in Section 6.1. We then inspect how the super-Earth and sub-Neptune populations vary with stellar mass in Section 6.2.

6.1. Dependence of the Radius Gap on Period, Flux, Stellar Mass, and Stellar Metallicity

Figure 6 shows several views of our planet sample. The y-axes show updated Rp, and the x-axes show \( P, S_{\text{inc}}, M_s, \) and [Fe/H]. The contours show the relative density of detected
Planets in these domains using a Gaussian kernel density estimation (KDE), and the KDE bandwidths are specified in the caption. Figure 7 is analogous to Figure 6 but with \( R_p \) restricted to 1–4 \( R_⊕ \) for a detailed view of the radius gap.

The \( P–R_p \) distribution and closely related \( S_{inc}–R_p \) distribution of Kepler planets have been extensively studied in previous works. We begin by remarking on several known features that appear in our extended stellar-mass sample. Most Kepler planets fall into one of two size categories: super-Earths and sub-Neptunes. For definitiveness, we adopt the following size limits for the two planet classes: \( R_p = 1.0–1.7 \) and 1.7–4.0 \( R_⊕ \). The radius gap separating the populations was observed by Fulton et al. (2017) in CKS DR1 (\( M_∗ \approx 0.8–1.3 M_⊙ \), Van Eylen et al. (2018) in a sample of stars with asteroseismic detections (\( M_∗ \approx 1.0–1.4 M_⊙ \)), and other subsequent works. We again resolve the radius gap, despite the broader \( M_∗ \) range of the CXM sample (\( M_∗ \approx 0.5–1.4 M_⊙ \)).

The distribution of super-Earths is centered at shorter periods and higher incident fluxes than the distribution of sub-Neptunes. Compared to super-Earths, there are few sub-Neptunes with \( P < 3 \) days or \( S_{inc} > 300 S_⊕ \). This paucity of sub-Neptunes is not a selection effect because larger planets are easier to detect. This zone of low sub-Neptune occurrence is sometimes referred to as the sub-Neptune desert (see, e.g., Szabó & Kiss 2011; Beaugé & Nesvorný 2013; Lundkvist et al. 2016). In Section 7, we quantify the sharpness of this boundary and explore its dependence on stellar mass. The relative lack of super-Earths at \( P > 30 \) days and \( S_{inc} < 10 S_⊕ \) is closely tied to survey completeness, also addressed in Section 7.

We wish to characterize the slope of the radius gap in \( P–R_p \) and \( S_{inc}–R_p \) space because it is a metric by which to test theoretical predictions. However, fitting a parameterized description of the radius gap is challenging, since it involves characterizing the absence of planets. Van Eylen et al. (2018) used a support vector classification (SVC) scheme to find the line that maximized the distance between the super-Earth and sub-Neptune populations. The SVC scheme struggles for our sample because the gap is not devoid of planets. (Recently, David et al. 2021 investigated how regularization can assist the SVC identification of the radius gap in the CKS sample.)

We adopted a different approach, starting with the relative number density of detected planets in the \( P–R_p \) plane \( d^2N/d\log R_p d\log P \) as measured by our KDE. This quantity is shown as contours in Figure 7(a). We then found the minimum density along 100 vertical lines spanning \( \log R_p = 0.15–0.35 \) spaced uniformly in \( \log P \) over 0.5–1.5.
We then fit the train of 100 minima with following power law:

\[ R_p(P) = R_{p,0} \left( \frac{P}{10 \text{ days}} \right)^m, \]  

where the slope \( m \) and intercept \( R_{p,0} \) are free parameters. To be clear, \( R_{p,0} \) should be interpreted as the midpoint of the radius gap at 10 day orbital periods. We chose 10 days as a convenient reference point near the middle of the super-Earth and sub-Neptune populations shown in Figure 7(a). To determine uncertainties, we generated 1000 bootstrap resamples with replacement of the planet population shown in Figure 7(a) (Press 2002). For each bootstrapped population, we recomputed the planet number density with our KDE, the train of minima, and the best-fitting power law. We found \( m = 0.11^{+0.02}_{-0.02} \) and \( R_{p,0} = 1.84^{+0.03}_{-0.03} R_\oplus \), which reflect the 16th, 50th, and 84th percentiles. Figure 7 shows the credible gap models. We explored the sensitivity of our method to different period ranges by perturbing the upper and lower boundaries by \( \pm 0.25 \) dex. The derived parameters were consistent to 1σ. We also explored the sensitivity of our method to our adopted KDE period bandwidth. A very wide bandwidth will flatten the radius gap (i.e., bias \( m \) toward smaller values). We repeated our analysis with a much smaller bandwidth of 0.04 dex and found that \( m \) and \( R_{p,0} \) changed by less than 1σ.

We performed similar analyses to fit the radius gap as a function of \( S_{\text{inc}}, M_*, \) and \([\text{Fe}/\text{H}]\). Table 3 lists the parametric models used in the fits and the credible range of parameters. Figure 7 shows the range of credible gap models. We observed a positive slope with incident flux \( (d \log R_p/d \log S_{\text{inc}} = 0.06^{+0.01}_{-0.01}) \), a positive slope with stellar mass \( (d \log R_p/d \log M_* = 0.18^{+0.08}_{-0.07}) \), and no significant correlation with metallicity \( (d \log R_p/d [\text{Fe}/\text{H}] = 0.01^{+0.05}_{-0.06}) \).

We explored how the \( P-R_p \) distribution of planets changes with \( M_* \). The left panels of Figure 8 shows this distribution for three different bins of stellar mass with the following boundaries: 0.5, 0.7, 1.0, and 1.4 \( M_\odot \). The super-Earth and sub-Neptune populations are distinct in each bin, but their locations vary with \( M_* \). As \( M_* \) increases, the population of super-Earths and sub-Neptunes separates; the super-Earth population is confined to \( R_p < 1.7 R_\oplus \) while the sub-Neptunes grow in size. We measured the slope and intercept of the radius gap in these three bins. They are given in Table 3 and consistent to 2σ.

We also explored how the \( S_{\text{inc}}-R_p \) distribution changes with \( M_* \). Figure 9 is analogous to Figure 8, except it shows the \( S_{\text{inc}}-R_p \) distribution for three bins of stellar mass. The credible models describing the radius gap in this space are consistent to 2σ.
6.2. Dependence of Planet Size on Stellar Mass

In the previous section, we measured the slope of the radius gap in the $R_p$–$M_\star$ plane and noted that it increases with $M_\star$. Inspecting Figure 7(c), we see qualitatively that the radius gap trend is driven by the fact that the typical sub-Neptune grows with stellar mass, while the typical super-Earth does not. Here we quantify these trends and explore possible confounding factors.

We first measured the sub-Neptune $R_p$–$M_\star$ correlation by selecting all sub-Neptunes from the population shown in Figure 7 based on their radii ($R_p = 1.7$–$4.0\ R_\oplus$). We then fit a power law,

$$R_p = R_{p,0} \left( \frac{M_\star}{M_\odot} \right)^\alpha.$$  

We used the Levenberg–Marquardt algorithm as implemented in the `lmfit` Python package to find the best-fit parameters and measured uncertainties via 1000 bootstrap resamples. We detected a positive correlation between $M_\star$ and sub-Neptune size at 8σ significance, $\alpha = 0.25 \pm 0.03$. An identical analysis for the super-Earths ($R_p = 1.0$–$1.7\ R_\oplus$) revealed no correlation, $\alpha = 0.02 \pm 0.03$.

Before interpreting these trends with $M_\star$, we must consider the confounding effects of other stellar properties that are correlated with $M_\star$. (We consider effects from the $M_\star$-dependent survey completeness in Section 7.2.) Stellar metallicity and age are both concerns because they are astrophysically correlated with mass. This $M_\star$–[Fe/H]–age correlation is tied to the chemical enrichment of the galaxy and stellar life spans. A star’s main-sequence lifetime is a strong function of its mass: $t_{\text{ms}} \sim 10 \text{ Gyr} \ (M_\star/M_\odot)^{-2.5}$. Massive stars are younger, on average, and formed when the galaxy was more enriched in metals, as shown in Figures 5(a) and (c). Figure 5(b) highlights the variable uncertainties of our age measurements, which range from $\approx 0.1$ dex for stars that have evolved off the main sequence to $\approx 0.5$ dex for stars with $T_{\text{eff}} \lesssim 5500$ K, i.e., indistinguishable from the zero-age main sequence.

We quantified possible metallicity and age effects by including them in our regression:

$$R_p = R_{p,0} \left( \frac{M_\star}{M_\odot} \right)^\alpha \left( \frac{N_{\text{Fe}}}{N_{\text{Fe},\odot}} \right)^\beta \left( \frac{\text{age}}{5 \text{ Gyr}} \right)^\gamma.$$  

When we allowed $\alpha$ and $\beta$ to vary and fixed $\gamma$ to zero, we found $\beta = -0.01 \pm 0.02$ and $-0.00 \pm 0.02$ for sub-Neptunes and super-Earths, i.e., no significant $R_p$–[Fe/H] correlation. Finally, we considered the effects of age by allowing $\gamma$ to vary as well. We restricted our analysis to stars with $T_{\text{eff}} > 5500$ K where age$_{\text{iso}}$ is not prior-dominated. We found $\gamma = -0.01 \pm 0.03$ and $0.02 \pm 0.02$ for the sub-Neptunes and super-Earths, i.e., no $R_p$–age correlation.

Based on these fits, we concluded that stellar mass rather than metallicity or age is the property most closely linked to...
measure the planet occurrence rate density (ORD), $d^2f/d\log P d\log R_p$. One may integrate the ORD over a specified domain in the $P$-$R_p$ plane to derive the number of planets per star residing in that domain.

For every detected planet in a sample of $n_\star$ stars, a large number are missed due to nontransiting geometries or insufficient photometric S/N. We account for both effects here using the inverse detection efficiency method (IDEM; see Fulton & Petigura 2018). Each detected planet $i$ with $(P, R_p)$ represents $w_i = 1/(p_{\star \text{det}})$ total planets, where $(p_{\star \text{det}})$ is the product of transit and detection probability averaged over the parent stellar population. We computed $(p_{\star \text{det}})$ over a grid of $(P, R_p)$. The probability that a randomly inclined planet with semimajor axis $a$ will transit with $b < 0.8$ is $p_a = 0.8 R_p a$, assuming circular orbits. We computed $p_a$ for each star using the B20 $R_\star$ and deriving $a$ from $P$ and the B20 $M_\star$ using Kepler’s third law.

We characterized the recovery rate $p_{\text{det}}$ following the procedure described in Christiansen et al. (2020). These authors injected a suite of 146,295 synthetic transits into the raw Kepler pixel-level data and searched for transits using the same pipeline used to produce the T18 catalog. The output was a list of injections that were either successfully recovered or not. This list may be used to determine the average recovery rate for any Kepler sample of interest. We selected the subset of injections with $P = 1$–300 days into our parent stellar population described in Section 2 and measured the recovery rate as a function of the expected MES, a close relative of transit S/N. We modeled the completeness curve as a $\Gamma$-cumulative distribution function:

$$p_{\text{det}}(\text{MES}) = \frac{c}{b^\Gamma(a)} \int_0^{\text{MES}} t^{a-1} e^{-tb} dt.$$  

The best-fit model had the coefficients $(a, b, c) = (26.1, 0.320, 0.941)$ and is shown in Figure 10. We set the recovery rate to zero when MES < 10 to incorporate our filter described in Section 2. We evaluated the MES for each star based on the putative planet’s transit depth and duration and the star’s tabulated photometric noise (combined differential photometric precision; Jenkins et al. 2010).

With our calculated weights $w_i$, we may now compute the total number of planets within a given region of the $P$-$R_p$ plane by summing the weights of the planets within that region, $\sum w_i$, or compute the occurrence rate (number of planets per star) via $(1/n_\star)\sum w_i$.

The IDEM, while mathematically straightforward, has some drawbacks, particularly when $p_{\text{det}}$ is small. In brief, Hsu et al. (2018) showed that the IDEM is a biased estimator at low $p_{\text{det}}$ because the weights $w_i$ are computed assuming no uncertainties in $R_p$. Hsu et al. (2018) proposed a less biased estimator using approximate Bayesian computation (ABC). We avoided these complications by restricting our analysis to regions where $p_{\text{det}} > 25\%$, where differences between the IDEM and ABC amount to $<1\sigma$ (Fulton & Petigura 2018).

We measured the ORD in the three bins of stellar mass introduced in Section 6.2 via

$$\frac{df}{d\log P d\log R_p} = \frac{1}{n_\star} \sum_i w_i k(P - P_i, R_p - R_{p,i}),$$  

where $k$ is a 2D Gaussian with a bandwidth of $\log(2) = 0.3$ dex in $P$ and $\log(1.05) = 0.02$ dex in $R_p$. The results are shown in

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### Table 3

| Fit | $M_\star$ | $m$ | $R_p$ | Dist. |
|-----|-----------|-----|-------|------|
| $R_p = R_{p,0} \left( \frac{P}{70 \text{ days}} \right)^{M_\star}$ | 0.5–1.4 | $-0.11^{+0.02}_{-0.02}$ | $1.84^{+0.03}_{-0.03}$ | D |
| 0.5–0.7 | $-0.12^{+0.06}_{-0.06}$ | $1.76^{+0.05}_{-0.06}$ | D |
| 0.7–1.0 | $-0.13^{+0.07}_{-0.06}$ | $1.74^{+0.09}_{-0.08}$ | D |
| 1.0–1.4 | $-0.06^{+0.02}_{-0.02}$ | $1.93^{+0.04}_{-0.04}$ | D |
| 0.5–0.7 | $-0.06^{+0.04}_{-0.05}$ | $1.71^{+0.05}_{-0.04}$ | O |
| 0.7–1.0 | $-0.10^{+0.07}_{-0.05}$ | $1.70^{+0.09}_{-0.10}$ | O |
| 1.0–1.4 | $-0.05^{+0.03}_{-0.03}$ | $1.93^{+0.06}_{-0.05}$ | O |
| 0.5–1.4 | $0.06^{+0.01}_{-0.01}$ | $1.86^{+0.04}_{-0.03}$ | D |
| 0.5–0.7 | $0.07^{+0.02}_{-0.03}$ | $2.00^{+0.11}_{-0.19}$ | D |
| 0.7–1.0 | $0.10^{+0.04}_{-0.04}$ | $1.86^{+0.07}_{-0.07}$ | D |
| 1.0–1.4 | $0.05^{+0.01}_{-0.01}$ | $1.85^{+0.04}_{-0.04}$ | D |
| 0.5–0.7 | $0.06^{+0.02}_{-0.02}$ | $1.93^{+0.11}_{-0.11}$ | O |
| 0.7–1.0 | $0.08^{+0.04}_{-0.04}$ | $1.81^{+0.08}_{-0.08}$ | O |
| 1.0–1.4 | $0.05^{+0.01}_{-0.01}$ | $1.84^{+0.04}_{-0.04}$ | O |
| 0.5–1.4 | $0.18^{+0.08}_{-0.07}$ | $1.86^{+0.03}_{-0.03}$ | D |
| $R_p = m \left( \frac{M_\star}{1 M_\odot} \right)^m$ | 0.5–1.4 | $0.01^{+0.05}_{-0.06}$ | $1.89^{+0.05}_{-0.03}$ | D |

Note. We fit the radius gap in the detected planet population in Section 6.1 as a function of orbital period, incident stellar flux, stellar mass, and stellar metallicity (see Figure 7). We repeated the orbital period and incident flux fits for narrower ranges of stellar mass (see Figures 8 and 9). We fit the radius gap in the debiased planet occurrence distribution in Section 7.1 (see Figures 8 and 9). We elaborate on the following columns: “Fit” is the functional form of the fit. “$M_\star$” is the range of stellar masses, and “Dist.” indicates whether the fit was of the distribution of planet detections “D” or occurrence “O.”

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7. Debiased Distribution of Planets

We have characterized the location and slope of the radius gap and its dependence on stellar mass. However, one must exercise caution when connecting these trends to planet formation models because the distributions of planets have been filtered through Kepler’s selection function. In this section, we remove selection effects to characterize variation in the planet population with stellar mass.

In Section 7.1, we reexamine the slope of the radius gap as a function of period and incident flux (first treated in Section 6.2) and find consistent results after accounting for selection effects. In Section 7.2, we measure the sizes of super-Earths and sub-Neptunes (as in Section 6.2) and observe the same qualitative trends after removing selection effects. In Section 7.3, we characterize how the period and incident flux distributions of super-Earths and sub-Neptunes vary with stellar mass.

### 7.1. Dependence of the Radius Gap on Stellar Mass

We return to the $P$-$R_p$ distribution of planets shown in Figure 8. We wish to remove Kepler’s observational biases to sub-Neptune size variation. We acknowledge two additional caveats to the above analysis, which we address in later sections. First, we fit the population of detected planets, which includes survey completeness effects that are addressed in Section 7.2. Second, orbital period is another possible confounding variable if the shape of the period distribution varies with stellar mass. Fortunately, as we show in Section 7.3, the period distribution is nearly independent of stellar mass up to a normalization constant.
the right panels of Figure 8. The value at each \((P, R_p)\) is the number of planets per star in a 1 dex \(\times\) 1 dex interval centered at \((P, R_p)\). It is convenient to scale this value to smaller intervals because the ORD varies significantly over 1 dex in \(P\) and \(R_p\). For example, to read off the number of planets per star within a box having the dimensions of the kernel FWHM, multiply the ORD by \(2.355 \times 0.3 \times 2.355 \times 0.02 = 0.033\).

We do not plot occurrence in regions of low planet detectability, defined to be where \(n_s(P, R_p) < 50\). The ORD ranges from \(\approx 0\) to 4, which corresponds to \(\approx 0–0.1\) planets star\(^{-1}\) within the kernel FWHM. For \((P, R_p)\) values where \(n_s(P, R_p) = 50\), there are effectively 50 stars where such a planet could be detected, and we would expect zero to five detected planets within the kernel FWHM. At this point, Poisson fluctuations become unmanageable.

We fit a power law to the radius gap for each mass bin. Our methodology, power-law parameterization, fitting domain, and uncertainty analysis are identical to those presented in Section 6, except that we fit ORD rather than the density of the detected planets. The credible range of values is given in Table 3. The measured slope and intercepts are consistent at 1\(\sigma\) to those measured using planet detections only.

7.2. Dependence of Planet Size on Stellar Mass

In Section 6.2, we noted a positive \(R_p-M_*\) correlation for sub-Neptunes that was not mirrored by super-Earths. However, we must consider the possibility that such correlations (or lack thereof) could stem from the Kepler selection function. To do so, we first divided the CXM planet hosts and parent stellar population into our three \(M_*\) bins from Section 6.2. In order to treat hosts and nonhosts equally, we used the B20 \(M_*\), which is available for all stars.

Returning to our binned planet population, we computed the occurrence-weighted mean planet sizes for sub-Neptunes
having $P < 100$ days and display them in Figure 11. Fitting the power law given by Equation (6) to the three binned mean size measurements shown in Figure 11 yields an index $\alpha = 0.23 \pm 0.04$ and an intercept of $R_{p,0} = 2.47 \pm 0.03$ $R_\oplus$ (uncertainties from bootstrap resampling). These values are consistent with our fits to the population of detected planets (Section 6.2). For the sub-Neptunes, the weights $w$ are dominated by geometrical corrections that are independent of $R_p$. Planets with larger $P$ have larger $w$ and are more strongly weighted than in Section 6.2. However, given the lack of a significant tilt in the $P$–$R_p$ distribution, the average value is similar.

Corrections stemming from low detectability are larger for the super-Earths. While there is no obvious tilt of the super-Earth population in Figure 7(c), completeness effects could conspire to produce a flat dependence when there is actually a positive slope in the underlying population. We computed the occurrence-weighted mean planet size for super-Earths with $P < 30$ days and found $\alpha = -0.01 \pm 0.03$ and $R_{p,0} = 1.34 \pm 0.01$, i.e., no significant correlation. We interpret the different $R_p$–$M_\star$ correlation super-Earths and sub-Neptunes and compare our results to previous literature measurements in Section 8.

7.3. Orbital Period and Incident Flux Distributions

One key feature of the exoplanet population is the paucity of sub-Neptunes with $P \lesssim 10$ days, i.e., the "sub-Neptune desert." The edge of this desert is significant in both the core- and XUV-powered models. It represents a boundary, inside of which core-dominated planets (i.e., $M_\star \gg M_{\text{env}}$) cannot retain H/He envelopes and are completely stripped.

Here we characterize the edge of the sub-Neptune desert in terms of period and flux and note how it changes with stellar mass. One can see qualitatively from Figures 8 and 9 that the edge of the sub-Neptune desert occurs at a similar $P$ for all mass bins but varies in $S_\text{inc}$ by $\sim 10 \times$. We first considered the edge in period space in our three bins of stellar mass introduced in Section 6.2. Quantitatively measuring this boundary in $P$ by visually inspecting Figure 8 is suboptimal for a number of

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Figure 9. Same as Figure 8, except the $x$-axis is incident bolometric flux.
reasons. First, the contours do not convey uncertainties. Second, the Gaussian KDE used to generate the 2D distributions smears out sharp features in the $P$ distributions. Third, the sub-Neptune desert is the paucity of short-period sub-Neptunes relative to long-period sub-Neptunes, but the contours show absolute occurrence, which also varies with stellar mass. These shortcomings motivated a different method, which we describe below.

Within each $M_*$ bin, we modeled the ORD as

$$\frac{df}{dPdR_p} = f_* \lambda(P, R_p; \theta)$$

over a rectangular domain of $P$ and $R_p$. Here $f_*$ is the mean number of planets per star within the $P$−$R_p$ domain. In principle, $\lambda$ may be any function that integrates to unity over the same domain. We consider parametric functions described by a vector of parameters $\theta$ that we will constrain through Bayesian inference. In short, the free parameters $f_*$ and $\theta$ control the normalization and shape of the ORD, respectively.

Following previous works, we modeled the detected population of planets as a realization of an inhomogeneous Poisson point process (see, e.g., Rogers & Owen 2021, and references therein). The log-likelihood of observing the full sample is given by

$$\ln L = -\Lambda + \sum_i \ln [f_*(P_i, R_p,i)],$$

where

$$\Lambda = n_* f_* \int \eta(P, R_p) \lambda(P, R_p) dPdR_p$$

is the expected number of detected planets given $f_*$ and $\theta$. Here $\eta = \langle p_d p_{\text{det}} \rangle$.

For simplicity, we assumed that the period and radius distributions are independent, i.e., $\lambda(P, R_p) \propto \lambda(P) \lambda(R_p)$. We also approximated the $R_p$ distribution log-uniform within the $R_p$ boundaries, i.e., $\lambda(R_p) \propto 1/R_p$. We precomputed

$$\eta(P) = \frac{1}{\Delta \ln R_p} \int \eta(P, R_p) d \ln R_p$$

$$\Lambda = n_* f_* \int \eta(P, R_p) \lambda(P, R_p) dPdR_p$$

(12)

(13)

(14)

(15)

where $C$ is the constant of proportionality that enforces normalization. In this parameterized description, $P_0$ is the knee of the distribution; for $P \ll P_0$ the distribution approaches a power law with an index of $k_1$, and for $P \gg P_0$, the index is $k_2$.

We first fit the sub-Neptune distribution for our three bins of stellar mass over $P = 1–300$ days. Our goal was to characterize the knee and slope of the occurrence period distribution. For consistency between the subsamples, we fixed $k_2 = -1$, i.e., log-uniform occurrence for $P \gg P_0$. We maximized the likelihood (Equation (11)) using the L-BFGS-B algorithm and explored the credible range of parameters using the MCMC sampler of Goodman & Weare (2010). We imposed log-uniform priors on $f_*$ and $P_0$ and a linear prior on $k_1$. We sampled the posterior with eight walkers for 5000 steps each and discarded the first 1000 as burn-in. The chains for all

21 The normalization constant $C$ is

$$C = \frac{P_0^{k_1+1}}{k_1+1} F_1 \left( 1, k_1 + 1; k_1 + 1; -u^{k_1-k_2} \right)$$

where $F_1$ is the hypergeometric function.
parameters were at least 50 times longer than the integrated autocorrelation time, indicating convergence. Table 4 lists the 16th, 50th, and 84th percentiles of our posterior samples. Figure 12 shows the posterior probability density of $f_s$ and $P_0$ for different $M_*$ bins.

Figure 13 shows the best-fit and credible range of models for our three $M_*$ bins. They are similar except for an overall shift in the normalization. For the low-, medium-, and high-mass bins, the breakpoint $P_0$ is at $7.0^{+1.4}_{-1.3}$, $9.7^{+2.9}_{-2.3}$, and $8.6^{+1.6}_{-1.3}$ days, respectively, consistent to $2\sigma$. The power-law indices $k_1$ agree to $1\sigma$ and are $1.7^{+0.5}_{-0.4}$, $1.5^{+0.4}_{-0.3}$, and $2.5^{+0.6}_{-0.5}$, we observed a steady decrease in the absolute number of planets per star from 0.5 to 1.4 $M_*$, of $1.3^{+0.19}_{-0.18}$, to $0.79^{+0.08}_{-0.08}$, to $0.6^{+0.05}_{-0.05}$.

The similarity of $P_0$ for the different mass bins is noteworthy because it indicates a key boundary in the planet formation process that is stationary over a wide range of stellar mass. Naturally, a stationary $P_0$ implies a variable $S_{inc,0}$ given the relationship between $M_*$ and bolometric luminosity. To quantify this boundary in flux space, we again characterized the distribution as a smooth broken power law,

$$\lambda(S_{inc}) = \frac{C}{(S_{inc}/S_{inc,0})^{-k_1} + (S_{inc}/S_{inc,0})^{-k_2}},$$

but fixed $k_1$ to $-1$. Over the three $M_*$ bins, we observed a factor of 9 increase in the breakpoint $S_{inc,0}$ from $27^{+16}_{-6}$, to $70^{+16}_{-13}$, to $244^{+55}_{-55}$ $S_{inc,0}$.

We also characterized the period distribution of super-Earths. Our modeling was identical to that of the sub-Neptunes, except we only included planets out to 30 days due to low completeness at longer orbital periods. Here the breakpoint $P_0$ increases with $M_*$ from $2.6^{+2.8}_{-0.8}$, to $3.3^{+1.3}_{-0.5}$, to $5.2^{+1.3}_{-0.9}$ days. The breakpoints in flux $S_{inc,0}$ occur at $89^{+35}_{-31}$, $265^{+76}_{-70}$, and $615^{+159}_{-152}$ $S_{inc,0}$.

Figure 14 contrasts the super-Earth and sub-Neptune breakpoints. The super-Earth breakpoint is shifted to smaller orbital periods and higher incident fluxes for all stellar-mass bins. We interpret these shifts in Section 8.5.

### 8. Discussion

#### 8.1. Positive $M_*$–$R_p$ Correlation Suggests Massive Stars Make Massive Planet Cores

One of the striking features of Figure 7 is the divergence of the super-Earth and sub-Neptune populations with stellar mass; the sub-Neptunes grow larger, while the super-Earths do not. When we modeled the size dependence of each population as a power law, $R_p \propto M_*^{\alpha}$, we found $\alpha = 0.25 \pm 0.03$ and $0.02 \pm 0.03$, respectively. The slope of the radius gap in $M_*$–$R_p$ space (displayed in Figure 7) lies between those two values, $m = 0.18^{+0.08}_{-0.07}$.

A positive sub-Neptune $R_p$–$M_*$ correlation has been noted in several previous works. Fulton & Petigura (2018) observed such a trend over a narrower stellar-mass range of $0.8$–$1.3 M_0$. Later, Wu (2019) stitched together the Fulton & Petigura (2018) sample with a compilation of $\sim 100$ Kepler and K2 planets with hosts of $M_\leq 0.7 M_0$ from Newton et al. (2015) and Dressing et al. (2017) and reported $\alpha = 0.23$–$0.35$, consistent with what we found.

In contrast to the sub-Neptunes, we observe a flat super-Earth $R_p$–$M_*$ dependence, $\alpha = -0.01 \pm 0.03$. This result differs from that of Wu (2019), who reported $\alpha = 0.23$–$0.35$. As a point of comparison, Figure 11 shows our occurrence-weighted mean super-Earth size with an $\alpha = 0.25$ dependence over-plotted; such a strong relationship is ruled out at $8\sigma$ significance. The differences between the two works may stem from the fact that Wu (2019) used an admixture of planet samples with heterogeneously derived properties.

Berger et al. (2020a) offered a second point of comparison. They derived properties of 2956 KOIs spanning $M_\approx 0.6$–$1.4 M_0$ that host 3898 confirmed/candidate planets. They measured the radius gap slope in $M_*$–$R_p$ space and found $m = 0.26^{+0.21}_{-0.16}$, which is consistent with our measured value, albeit with larger uncertainties.

What causes the super-Earth size to be independent of stellar mass while the sub-Neptune size grows with stellar mass? In our discussion below, we assume that planets between 1 and 4 $R_\oplus$ are Earth-composition bodies that may also include an H/He envelope. This assumption is supported by the growing body of mass measurements of planets in this size range (see, e.g., Weiss & Marcy 2014; Sinukoff 2018). Most planets smaller than 1.5 $R_\oplus$ have densities consistent with Earth-composition bodies; most planets larger than 2.0 $R_\oplus$ are too low-density to be rock/iron bodies and are consistent with having H/He envelopes of $f_{env} \geq 1\%$ by mass.

With this two-component model, both the XUV- and core-powered models produce the radius gap. In the 1D, energy-limited, XUV-powered models of Owen & Wu (2017), the mass-loss timescale $\tau_{XUV} = M/M$ is a strong function of $f_{env}$ and the local XUV flux. This timescale is maximized when the size of the core and thickness of the envelope are approximately equal, i.e., $R_p \approx 2R_\oplus$. This occurs at $f_{env,2} \approx 3\%$. Planets with less envelope experience accelerating mass loss; those
Figure 12. Panel (a): posterior probability density of the mean number of sub-Neptunes per star \( f_\alpha \) with \( P = 1–300 \) days for three stellar-mass bins. Dashed lines show the 25%, 50%, and 75% quantiles. Panel (b) shows the period breakpoint \( P_\alpha \). Panel (c) shows the flux breakpoint \( S_\text{inc,0} \). Panels (d)–(f) are the same as panels (a)–(c) but for super-Earths. The mean occurrence in panel (d) corresponds to \( P = 1–30 \) days. For both classes of planets, there is a decline in total occurrence with increasing \( M_* \). For the sub-Neptunes, \( P_\alpha \) ranges from \( \approx 7.0 \) to 9.6 days, consistent to 40%; for the super-Earths, \( P_\alpha \) is \( \approx 2.7–5.1 \) days, consistent to a factor of 2. For the sub-Neptunes, the breakpoint \( S_\text{inc,0} \) increases by a factor of 9 from \( 27^{+8}_{-6} \) to \( 244^{+44}_{-34} \) \( S_\odot \) between the low- and high-mass bin. For the super-Earths, the breakpoint also increases with stellar mass from \( 89^{+35}_{-26} \) to \( 615^{+157}_{-120} \) \( S_\odot \), a factor of 7 increase.

with more experience decelerating mass loss. Planets are herded toward \( f_\text{env} = f_\text{env,2} \) or \( f_\text{env} = 0 \) (bare cores).

In the XUV model, the fate of a planet’s envelope depends on the time-integrated XUV exposure \( F_{\text{xuv}} = \int F_{\text{xuv}} \, dt \). This quantity is strongly correlated with orbital period and weakly correlated with stellar mass (Owen & Wu 2017). At a fixed orbital period, planets around low-mass stars receive less bolometric flux \( F_{\text{bol}} \), but \( F_{\text{xuv}} / F_{\text{bol}} \) is higher, and stars stay XUV-active longer. McDonald et al. (2019) found \( F_{\text{xuv}} \propto F_{\text{bol}} M_*^{-3} \). Applying the following relationships, \( P^2 \propto a^3 / M_* \) (Kepler’s third law), \( F_{\text{bol}} \propto L_{\text{bol}} / a^2 \), and \( L_{\text{bol}} \propto M_*^4 \) (Kippenhahn & Weigert 1990, for FGK and early M stars), we find \( F_{\text{xuv}} \propto M_*^{0.33} P^{-1.33} \).

If the XUV model is correct and the initial planet population is independent of \( M_* \), we expect only minor sub-Neptune size variability with \( M_* \). We can get a rough estimate of the expected \( R_p - M_* \) dependence at fixed \( P \) by considering the amount of energy needed to unbind an \( f_\text{env} \approx 3\% \) envelope:

\[
E_{\text{ubn}} \sim G M_* M_{\text{env}} / R_p \propto M_*^{1.75}.
\]  

We have approximated the rocky mass–radius relationship as \( R_c \propto M_*^{0.25} \). The XUV energy received by the planet is approximately

\[
E_{\text{rec}} \sim F_{\text{xuv}} \pi R_p^2 \propto F_{\text{xuv}} M_c^{0.5} \propto M_*^{0.33} M_c^{0.5}.
\]

Equating the two energies yields \( M_c \propto M_*^{0.26} \) or \( R_c \propto R_p \propto M_*^{0.06} \), i.e., \( \alpha \approx 0.06 \).

In the core-powered model of Gupta & Schlichting (2020), planets with \( f_{\text{env}} < 5\% \) have enough thermal energy in their cores to unbind their envelopes and become bare rocky planets. Thus, this process also works to clear the \( P-R_p \) plane of planets with an \( f_{\text{env}} \) of a few percent or less. The fate of a planet’s envelope depends on the mass flux at the Bondi radius \( R_B \), and planets with smaller \( R_B \) lose mass faster. Since \( R_B \propto M_* / T_{\text{eq}} \), planets more readily lose their envelopes when \( T_{\text{eq}} \) (or, equivalently, \( S_{\text{inc}} \)) is large or \( M_* \) is small. If the core-powered model is correct and the initial planet population is independent of \( M_* \), we expect significant changes with \( M_* \) because \( S_{\text{inc}} \) is a strong function of \( M_* \). Gupta & Schlichting (2020) predicted \( \alpha \approx 0.33 \).

It is tempting to interpret the larger sub-Neptunes around massive stars as a direct result of higher-mass cores. One may, for example, adopt a monotonically increasing mass–radius relationship (e.g., Weiss & Marcy 2014), invert it, and infer higher-mass sub-Neptunes around more massive stars. However, there is significant astrophysical scatter about the mean
mass–radius relationship (Wolfgang et al. 2016). Planets of \(2–3 R_\oplus\) have a nearly uniform distribution in mass from 5 to \(20 M_\oplus\). In short, radius is not a good predictor of mass. It could also be true that faster or more efficient gas accretion occurs in the protoplanetary disks of massive stars because of differences in gas surface density, ionization structure, or other properties.

With these caveats in mind, we can qualitatively explain the increase in sub-Neptune sizes and constant super-Earth sizes in both XUV- and core-powered models as a consequence of more massive cores around more massive stars. We first consider photoevaporation in a toy model shown in Figure 15. Here the cores have a log-uniform mass distribution up to a maximum cutoff mass of \(M_{c,max}\). The maximum core mass is proportional to stellar mass, \(M_{c,max} \propto M_*\). For simplicity, we show two populations of host stars: (1) where \(M_{c,1} \approx 0.6 M_\odot\) and \(M_{c,max,1} \approx 10 M_\oplus\) and (2) where \(M_{c,2} \approx 1.2 M_\odot\) and \(M_{c,max,2} \approx 20 M_\oplus\). At the time of disk dispersal (\(t \sim 10\) Myr), the cores have accreted H/He envelopes with a broad range of \(f_{env} \approx 0.3\%–30\%\) and have a broad size distribution \(R_p \approx 2–10 R_\oplus\).

After the period of high XUV activity (\(t \gtrsim 100\) Myr), cores up to a critical mass \(M_{c,crit}\) are stripped bare, and the largest super-Earth is given by \(R_{se,\max}/R_\oplus \approx (M_{c,crit}/M_\oplus)^{0.25}\). Cores above \(M_{c,crit}\) retain their envelopes, and mass loss concentrates envelope fractions to \(f_{env} \approx 3\%\). The smallest sub-Neptunes have cores that barely retained their envelopes and obey \(R_{se,\min}/R_\oplus \approx 2(M_{c,crit}/M_\oplus)^{0.25}\); the largest sub-Neptunes have an \(f_{env} \approx 3\%\) envelope atop an \(M_{c,\max}\) core and obey \(R_{se,\max}/R_\oplus \approx 2(M_{c,\max}/M_\oplus)^{0.25}\).

This toy model reproduces some, but not all, of the observed trends. Here \(M_{c,\max} \propto M_*\), so \(R_{se,\max} \propto M_*^{0.25}\), which is consistent with the observed trend. Moreover, approximating \(f_{env} \propto M_*^{0.33}\) as constant over our mass range predicts a constant \(R_{se,\max}\) for different \(M_*\).

The fact that \(R_{se,\max} \approx 1.7 R_\oplus\) implies \(M_{c,crit} \approx 8 M_\oplus\) and \(R_{se,\min} \approx 3.4 R_\oplus\). Given our assumed \(M_{c,\max}\), we find \(R_{se,\max} \approx 3.6\) and \(4.2 R_\oplus\). While these have the appropriate dependence on \(M_*\), they exceed the upper envelope of the observed sub-Neptunes. Note, however, that these sizes are at \(t \sim 100\) Myr, and the observed planets are \(t \approx 1–10\) Gyr and will contract as they radiate away their heat of formation. Gupta & Schlichting (2020) found that the radius of the radiative–convective boundary (RCB) shrinks as \(d \log R_p/d \log t \approx -0.1\). So, over \(\log t = 8–9.7\), we expect the planets to shrink by 0.17 dex or 33\%. The largest sub-Neptunes would shrink to 2.2 and 2.8 \(R_\oplus\) for the \(M_{c,1} \approx 0.6\) and \(M_{c,2} \approx 1.2 M_\odot\) populations, respectively, in rough agreement with

![Figure 13](https://example.com/figure13.png)

**Figure 13.** Panel (a): period distribution of sub-Neptunes for three bins of stellar mass. The points show the number of planets per star in period bins that are 0.25 dex wide: We modeled the ORD \(df/dP\) as a smooth broken power law, which we fit to the unbinned planet population over \(P = 1–300\) days (see Section 7.3). The bands show the credible range of \(df/d \log P \times 0.25\) dex. The height of each curve at a particular \(P\) is the number of planets per star within a 0.25 dex period interval centered at \(P\). Panel (b): same as panel (a) except for super-Earths where the fits extend to 30 days. Panels (c) and (d): same as panels (a) and (b) except showing incident flux distribution. The vertical axis has the following interpretation: number of planets per star within a 0.5 dex flux interval.
observations. However, we note that we observed no age dependence in the mean sub-Neptune size over log $t = \pm 9-10$, and we comment on this discrepancy later.

Given the similarities between the core- and XUV-powered models, this toy model may be easily adapted to the core-powered model. The key difference is that the time of rapid mass loss is $t \lesssim 1$ Gyr, as opposed to $t \lesssim 100$ Myr.

To summarize, the $R_p-M_*$ correlation observed for super-Earths and sub-Neptunes is broadly consistent with a maximum core mass that increases with $M_*$. The $R_p \propto M_*^{0.25}$ trend suggests an $M_c \propto M_*$ relationship. A linear relationship between core mass and host star mass has also been suggested by Wu (2019) and Berger et al. (2020a).

Why should core mass increase with host star mass? One explanation could be that the core formation process is dust-limited and that the available dust mass $M_{\text{dust}}$ grows with stellar mass. Pascucci et al. (2016) derived $M_{\text{dust}}$ in protoplanetary disks from ALMA observations at $\sim 1$ mm and found a superlinear relationship with stellar mass $M_{\text{dust}} \propto (M_*)^{1.3}$. With a large 0.8 dex dispersion about this relationship. It is not clear, however, if core formation is dust-limited due to the difficulties of inferring the total inventories of solids from millimeter emission. Wu (2019) offered a different interpretation, positing that planet cores form at a “thermal mass” $M_{\text{th}}$, the mass at which a planet’s Hill sphere equals the disk scale height, $M_{\text{th}} \propto M_*^{11/8}$, which is close to the inferred $M_c \propto M_*$ dependence.

8.2. Absence of Size–Metallicity Trend Suggests Weak Connection between Envelope Opacity and Stellar Metallicity

Models of sub-Neptunes depend on the envelope opacity $\kappa$, which sets the cooling rate and location of the RCB and thus the planet’s size. Higher-opacity envelopes cool and contract more slowly.

In their core-powered models, Gupta & Schlichting (2020) assumed $\kappa \propto Z$, where $Z$ is the bulk stellar metallicity. To isolate the effects of metallicity, they constructed a population of planets with $M_*$ fixed at $1.0 M_\odot$ and [Fe/H] ranging from $-0.5$ to $+0.5$ and evolved them for 3 Gyr. The final population is shown in their Figure 9 and reproduced here in Figure 16. In the models, sub-Neptune size increases with stellar metallicity as $R_p \propto Z^{0.5}$, with $\beta = 0.1$. In contrast, in Section 6.2, we measured $\beta = -0.01 \pm 0.02$, which rules out the predicted $\beta = 0.1$ at 4$\sigma$ significance.

For visual comparison, we reproduced Figure 7(d) in Figure 16 with a $\beta = 0.1$ relationship overplotted. The CXM distribution is peaked near [Fe/H] = 0.0, but no tilt is observable. To visually enhance the tails of the metallicity distribution, we normalized the density by the integrated density along vertical columns. Both super-Earths and sub-Neptunes show no significant size–metallicity dependence.

Our results suggest that the dominant opacity at the RCB does not track stellar metallicity. The tension between the observations and the Gupta & Schlichting (2020) model does
not reflect an insurmountable obstacle for core-powered theory but does suggest a modification to the opacity treatment. We also note that the XUV-powered models of Owen & Wu (2017) also assumed a $\kappa \propto T$ relationship.

### 8.3. Age Effects

After the period of rapid mass loss, we expect the sizes of the sub-Neptunes to decrease due to the Kelvin–Helmholtz mechanism. In Section 6.2, we found $R_p \propto (\text{age}/5 \text{ Gyr})^{-\gamma}$ with $\gamma = -0.01 \pm 0.03$, consistent with no $R_p$-age collocation. This flat age dependence is interesting given that several studies have noted that planets younger than 100 Myr seem to have inflated envelopes. In a recent compilation of nine planets with cluster-based ages under 100 Myr by Bouma et al. (2020), all were between 4 and 10 $R_\oplus$. Rizzuto et al. (2018) and David et al. (2019) made a similar observation among earlier compilations.

Planets in this size range are even rarer among low-mass stars. Dressing & Charbonneau (2013) measured an occurrence rate of 0.007 planets star$^{-1}$ with $R_p = 4.0–11.3 R_\oplus$ and $P < 50$ days in a sample of stars with $M_* \approx 0.4–0.6 M_\odot$. Yet K2-33 is a 5–10 Myr, 0.4$M_\odot$ star that hosts a 6$R_\oplus$ planet (David et al. 2016).

Given the evidence for inflated planets younger than 100 Myr in the literature combined with the flat $R_p$-age relationship observed here for ages spanning 1–10 Gyr, we conclude that large-scale evolution in the size of sub-Neptune envelopes concludes by $\sim$1 Gyr.

The envelopes may continue to contract after $\sim$1 Gyr, but the $R_p$-age trends may be too subtle to detect given our sample size and age uncertainties. For example, Gupta & Schlichting (2020) isolated the age effect in the core-powered context by constructing a planet population with $M_*$ and [Fe/H] held fixed at 1.0$M_\odot$ and 0.0 dex and evolved them from 1 to 10 Gyr (their Figure 10, reproduced here in Figure 16). In this model, the planets obeyed a $\gamma = -0.1$ relationship. However, errors in the measured ages will conspire to flatten such a trend. We explored this effect by injecting a $\gamma = -0.1$ dependence into the observed sub-Neptune population, perturbing their ages by their uncertainties, and refitting our power-law model. We found $\gamma = -0.06$, which is consistent with our measured value.
of $\gamma = -0.01 \pm 0.03$ at the $2\sigma$ level. Thus, we cannot rule out the subtle $\gamma = -0.1$ dependence predicted by Gupta & Schlichting (2020) given our current sample size and age uncertainties.

8.4. Slope of the Radius Gap in Period–Radius Space

While a number of theoretical models can produce the radius gap, they do not produce identical slopes in the $P$–$R_p$ plane. Thus, the slope of the radius gap has emerged as a potential discriminant between different models. In the Owen & Wu (2017) photoevaporation model, the maximum size of a super-Earth decreases with orbital period. The upper envelope is set by the size of a rocky core that is barely stripped by the integrated XUV exposure. Slightly more massive cores retain their envelopes and remain sub-Neptunes.

At larger orbital periods, $F_{\text{xuv}}$ decreases, and the cores that can be completely stripped have lower masses and smaller sizes. Assuming a fixed energy-limited efficiency factor $\eta = 10\%$, Owen & Wu (2017) predicted that the bottom of the radius gap will follow $R_p \propto P^m$ with $m = -0.25$. Realistically, $\eta$ should decline as mass increases, since escaping gas has more time to cool as it climbs out of a

![Figure 16](image-url)
deeper potential well. Adopting \( \eta = 10\% \left( v_{\text{esc}} / 15 \text{ km s}^{-1} \right)^{-2} \) yields a shallower slope, \( m = -0.16 \).

In the core-powered framework of Gupta & Schlichting (2019), the fate of an envelope around a planet with \( P \gtrsim 8 \) days depends on the cooling timescale \( t_{\text{cool}} = E / \text{L} \) relative to the envelope mass-loss timescale \( t_{\text{loss}} = M_{\text{env}} / \dot{M} \). Envelopes that escape faster than they cool, \( t_{\text{loss}} < t_{\text{cool}} \), are lost completely. The mass-loss timescale depends on \( \dot{M} \) at the Bondi radius, and \( t_{\text{loss}} \propto M_{\text{env}} R_{\text{c}, \text{rcb}}^2 c_s \exp \left( G M_p / c_s^2 R_{\text{rcb}} \right) \), where \( R_\text{c} \) is the sonic point and \( c_s \) is the sound speed. The cooling timescale may be computed by dividing the combined thermal and gravitational energy of the envelope and core by the luminosity evaluated at the RCB. The exponential behavior of \( t_{\text{loss}} \), results in the dividing line \( t_{\text{loss}} = t_{\text{cool}} \) being set by \( G M_p / c_s^2 R_{\text{rcb}} \) = constant, which implies \( R_p \propto P^{-0.11} \) or \( m = -0.11 \).

We emphasize that the values of \( m \) predicted by the core- and XUV-powered models discussed above have all incorporated assumptions about the properties of planet cores, such as the distribution of masses, orbital periods, and bulk compositions. Rogers et al. (2021) showed how changing these input parameters can alter the predicted \( m \). However, both the core- and XUV-powered models categorically predict a negative slope.

Models that delay the accretion of gas until the nebula is nearly or completely dissipated predict an increasing slope with orbital period. Here the core mass is determined by the solid surface density profile within a feeding zone that is proportional to the Hill radius \( R_H \propto a (M_*/M)^{1/3} \). A Hayashi (1981) profile \( \Sigma(a) \propto a^{-3/2} \) yields \( M_p \propto a^{0.6} M_*^{0.5} \), \( R_p \propto P^{0.11} M_*^{-0.09} \), or \( m = 0.11 \).

For the full CXM sample, we measured \( m = -0.11^{+0.02}_{-0.00} \). Van Eylen et al. (2018) fit the gap in a sample of 117 planets orbiting 75 stars with asteroseismic detections and found \( m = -0.09^{+0.02}_{-0.00} \). Their population of stellar hosts most closely resembles a combination of our middle- and high-mass bins, for which we measured \( m = -0.13^{+0.08}_{-0.06} \) and \( -0.06^{+0.02}_{-0.03} \), which straddle the Van Eylen et al. (2018) value. Martinez et al. (2019) performed an independent analysis of CKS DR1 spectra including parallax constraints and found \( m = -0.11 \pm 0.02 \). Despite differences in the planets used, planet/star parameter provenance, and slope measurement technique, our measurements of slope are consistent with the Van Eylen et al. (2018) and Martinez et al. (2019) measurements and the core- and XUV-powered model predictions.

Shifting our attention to low-mass stars, we resolved the radius gap among the 185 planets in our low stellar mass bin \( M_* = 0.5-0.7 M_\odot \). We measured \( m = -0.12^{+0.06}_{-0.04} \), consistent with that of the full sample. As a point of comparison, Cloutier & Menou (2020) measured the occurrence of planets in a sample of stars having \( T_{\text{eff}} < 4700 \text{ K} \) drawn from Kepler and K2 (275 and 53 planets). The host stars were \( M_* = 0.08-0.93 M_\odot \), but most were between 0.5 and 0.8 \( M_\odot \). They resolved the radius gap and measured a positive slope in \( P-R_p \) space of \( m = 0.058 \pm 0.022 \). They interpreted this as a signature of gas-poor formation channels around lower-mass stars. However, the radius gap is only visible in their full 328-planet sample, but not when they restrict their analysis to the 126 planets around \( M_* = 0.08-0.65 M_\odot \), hosts (their Figure 12). Our measured slope is \( \approx 4 \sigma \) lower than that of Cloutier & Menou (2020). We found no evidence of a change of slope and thus do not favor an alternate formation pathway for planets around \( M_* = 0.5-0.7 M_\odot \) stars. Van Eylen et al. (2021) arrived at a similar conclusion after analyzing a sample of 27 planets orbiting stars with \( T_{\text{eff}} < 4000 \text{ K} \).

Before concluding this section, we wish to remark on some of the challenges associated with using the slope of the radius gap as a signpost of formation. Note that our uncertainties on \( m \) are larger than those of Martinez et al. (2019), even though we resolved the valley at higher contrast (compare our Figure 7 to their Figure 12). One may understand this through the following limiting case. Consider super-Earth/sub-Neptune populations separated by a gap completely devoid of planets. In such a scenario, selecting the minima used to fit the radius gap in Section 6.1 is ill-posed because there is no longer a single minimum \( R_p \). Thus, a broad range of \( R_{p,0} \) and \( m \) are allowed. Thus, the statistic for assessing model predictions has the undesirable quality of becoming more uncertain as observational uncertainties improve.

Moreover, there is no standard approach to fitting the absence of planets. For example, Van Eylen et al. (2018) used a support vector machine scheme, Berger et al. (2020a) used the “gapfit” code that subtracts off a trial \( R_p \propto P^m \) relationship and evaluates a 1D KDE of the residuals, and Martinez et al. (2019) and this work fit a train of minima computed along 1D projections through the \( P-R_p \) plane. All approaches rely on an ad hoc smoothing parameter that determines the relative influence of the few planets near the edge of the gap relative to the many planets far from the gap on the fit. These differences in fitting method are less troublesome in theoretical studies that can model limitless numbers of planets and do not contend with complications like false-positive contamination or mischaracterized measurement uncertainties.

Recently, Rogers & Owen (2021) introduced a different framework for evaluating the agreement between formation theory and the observed planet population that does not rely on measuring the slope of the gap. Here a model planet population is subjected to a specified set of physical processes, e.g., XUV- or core-powered mass loss. The synthetic population is transformed into an ORD distribution. This is then converted into a number rate density distribution by accounting for properties of the parent stellar population and losses due to nontransiting planets and pipeline incompleteness. In this framework, one evaluates the likelihood that the observed planets are a realization of an inhomogeneous Poisson point process with the specified number rate density. One may then optimize the model parameters and characterize their uncertainties using standard techniques. Such a treatment of the CXM sample would be interesting but is beyond the scope of this paper.

8.5. Period–Flux Distribution of Planets

In Section 7.3, we characterized the period distribution of super-Earths and sub-Neptunes \( dN/dP \) in three bins of stellar mass. We parameterized these distributions as smooth broken power laws with variable breakpoints \( P_0 \). From \( M_* = 0.5 \pm 1.4 M_\odot \), the sub-Neptune falloff occurs at a nearly constant \( P_0 \approx 10 \) days. Similarly, when we modeled the flux distribution, \( dN/dS_{\text{inc}} \), we found that \( S_{\text{inc},0} \) increases by nearly an order of magnitude, from \( \approx 20 \) to 200 \( S_\odot \).

Under the assumptions that planet cores (1) are uniformly distributed in log-period and (2) have masses that are uncorrelated with \( M_* \), the above observation would be strong evidence for XUV-powered and against core-powered mass loss. As we explain in Section 8.1, \( F_{\text{xuv}} \propto M_*^{0.33} \) and thus only
varies by 40% over our full mass stellar range. Thus, the critical \( \mathcal{F}_{\text{XUV}} \) that strips the typical sub-Neptune maps to a \( P_0 \) that is constant with \( M_\star \). A fixed \( P_0 \) corresponds to an \( S_{\text{inc},0} \) that grows with \( M_\star \). Under the same assumptions, \( S_{\text{inc},0} \) should be constant with \( M_\star \) in the core-powered model.

Neither of the above assumptions, however, appear to be correct. The steep decline in super-Earths for \( P \leq P_0 \approx 5 \) days suggests that rocky cores struggle to form inside this boundary. Several mechanisms may be responsible, including magneto-spheric truncation of the inner disk (e.g., Lee & Chiang 2017) or a pressure trap due a silicate sublimation front (e.g., Flock et al. 2019). Moreover, the \( M_\star - R_\star \) correlation discussed in Section 8.1 suggests that massive stars make massive cores.

Therefore, we cannot rule out the core-powered model based on the dependence of \( P_0 \) and \( S_{\text{inc},0} \) on \( M_\star \). In this framework, stars that are 1.0–1.4 \( M_\odot \) efficiently produce sub-Neptunes when \( S_{\text{inc}} \leq S_{\text{inc},0} \approx 200 \) \( S_\odot \). Stars that are 0.5–0.7 \( M_\odot \) only efficiently produce sub-Neptunes when \( S_{\text{inc}} \leq S_{\text{inc},0} \approx 20 \) \( S_\odot \). The lack of sub-Neptunes in the \( S_{\text{inc}} \approx 20–200 \) \( S_\odot \) range is not due to envelope stripping but rather to the absence of suitable cores. Inspecting Figure 13, we see that the ORD of super-Earths declines by a factor of 5 over \( S_{\text{inc}} = 20–200 \) \( S_\odot \).

There is still considerable uncertainty in the distribution of core masses and further uncertainty in how that distribution varies with \( P \) and \( M_\star \). Given these unknowns, both core- and XUV-powered frameworks appear sufficiently flexible to match the observations. Additional mass measurements of sub-Neptunes as a function of \( P - S_{\text{inc}} - M_\star \) should help to constrain the models, since \( R_\star \) and \( M_\star \) together constrain both core mass and envelope fraction.

9. Summary and Conclusion

Here we provide a brief summary of our results and point toward future improvements to this work.

1. We augmented the 1305-star CKS DR1 spectral library with DR2 containing 411 new spectra.
2. We performed a homogeneous analysis of the combined DR1 and DR2 samples and derived \( T_{\text{eff}}, [\text{Fe/H}], \nu \sin i, M_\star, R_\star \), and age.
3. We constructed a curated sample of 970 planets orbiting 703 stars with updated star/planet properties.
4. We resolved the radius gap and projected the planet population as a function of \( P, S_{\text{inc}}, M_\star, [\text{Fe/H}], \) and age.
5. The radius gap in the \( P - R_\star \) plane follows \( R_\star \propto P^m \) with \( m = -0.10 \pm 0.03 \), consistent with both core- and XUV-powered models but inconsistent with gas-poor formation models.
6. We observed no significant change in \( m \) over 0.5–1.4 \( M_\odot \).
7. Sub-Neptunes tend to be larger around higher-mass stars and follow \( R_\star \propto (M_\star / M_\odot)^\alpha \) with \( \alpha = 0.25 \pm 0.03 \). The super-Earths exhibit no measurable \( M_\star \) dependence \( \alpha = 0.02 \pm 0.03 \). Taken together, these trends are consistent with a core mass distribution that scales linearly with stellar mass \( M_\star \propto M_\odot \).
8. The average sub-Neptune is not measurably larger around higher-metallicity stars, disfavoring a simple linear relationship between envelope opacity and stellar metallicity \( \kappa \propto Z \).
9. The average sub-Neptune does not measurably shrink over 1–10 Gyr. Given the large radii observed among stars younger than 100 Myr, we conclude that the majority of planet radius contraction concludes by ~1 Gyr.
10. The period distribution of sub-Neptunes has a breakpoint \( P_0 \) in \( M_\star \). This is consistent with the predictions of photoevaporation models. However, core-powered models may still be viable given the uncertainties in the underlying distribution of planet cores.

The bifurcation of small planets into two distinct populations was one of the most intriguing results from the Kepler mission. This feature appears most consistent with models where close-in planets acquire and lose \( H/He \) envelopes. The XUV radiation from young stars or heat from cooling cores are leading candidates for the energy source that powers this mass loss. While we worked to identify the dominant mass-loss process, we found that both mechanisms are flexible enough to match our observations.

We look forward to additional observational and theoretical work that could help discriminate between these two theories. With Gaia, it will soon be possible to extend the analysis presented here to a larger sample of planets (2–3×). Future Gaia data releases will include low- and high-resolution spectra for nearly all Kepler stars. These data will increase the upper \( M_\star \) limit, since rapid rotation above 6500 K does not wash out broadband spectral energy distribution information. Gaia-based refinements in \( T_{\text{eff}} \) and \([\text{Fe/H}]\) will be especially useful in determining masses and ages for additional early-type stars. However, increases in sample size from Gaia may not settle the core-powered versus XUV-powered question. An analysis of synthetic planet populations by Rogers et al. (2021) suggested that \( \geq 5000 \) planets are needed to do so.

We found that heuristic descriptions of the radius gap, such as its slope in the \( P - R_\star \) plane, were neither straightforward to compute nor straightforward to compare to model predictions, which are based on a previous occurrence analysis. The disconnect between the demographic analysis and the population modeling leads to concerns of self-inconsistency. The modeling approach of Rogers & Owen (2021) offers a firmer statistical basis for comparing models and observations. This approach can also naturally accommodate realistic non-independent distributions of host star properties like mass, metallicity, and age.

Aside from improved host star properties, additional planet observables should shed light on the mass-loss process. Mass measurements of transiting planets spanning \( P, S_{\text{inc}}, [\text{Fe/H}] \), and age will help constrain the core mass distribution that contributes to the remaining flexibility of both models, since mass and radius together constrain core mass and envelope fraction. Finally, direct measurements of mass loss as a function of the same properties would be especially valuable. Outflows from a handful of planets have been recently detected using the He 10830 Å line, and Gupta & Schlichting (2021) have highlighted a number of planets that may actively be experiencing mass loss in the core-powered framework.

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