REFINED ROTATIONAL PERIOD, POLE SOLUTION, AND SHAPE MODEL FOR (3200) PHAETHON

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ABSTRACT

(3200) Phaethon exhibits both comet- and asteroid-like properties, suggesting it could be a rare transitional object such as a dormant comet or previously volatile-rich asteroid. This justifies detailed study of (3200) Phaethon’s physical properties as a better understanding of asteroid–comet transition objects can provide insight into minor body evolution. We therefore acquired time series photometry of (3200) Phaethon over 15 nights from 1994 to 2013, primarily using the Tektronix 2048 × 2048 pixel CCD on the University of Hawaii 2.2 m telescope. We utilized light curve inversion to (1) refine (3200) Phaethon’s rotational period to \( P = 3.6032 \pm 0.0008 \) hr; (2) estimate a rotational pole orientation of \( \lambda = +85^\circ \pm 13^\circ \) and \( \beta = -20^\circ \pm 10^\circ \); and (3) derive a shape model. We also used our extensive light curve data set to estimate the slope parameter of (3200) Phaethon’s phase curve as \( G \sim 0.06 \), consistent with C-type asteroids. We discuss how this highly oblique pole orientation with a negative ecliptic latitude supports previous evidence for (3200) Phaethon’s origin in the inner main asteroid belt as well as the potential for deeply buried volatiles fueling impulsive yet rare cometary outbursts.

Key words: minor planets, asteroids: individual (3200 Phaethon) – techniques: photometric

Online-only material: supplemental data

1. INTRODUCTION

(3200) Phaethon is a unique minor body in the solar system, exhibiting both asteroid- and comet-like properties. For example, its unambiguous association with the Geminid meteor stream (Whipple 1983; Gustafson 1989; Williams & Wu 1993) strongly supports a cometary origin, as meteor streams are typically formed from debris left along comet orbits as a result of volatile-driven activity. However, comet-like activity has never been observed in (3200) Phaethon (Hsieh & Jewitt 2005; Wiegert et al. 2008), suggesting a more asteroid-like character (the recurrent dust tail at perihelion recently reported by Jewitt et al. 2013 is unlikely to result from volatile-driven activity). (3200) Phaethon also has features neither distinctly cometary nor asteroidal: its blue color fails to match the typical neutral/red colors of comet nuclei (Lamy et al. 2004) while its spectral shape fails to closely match any meteoritic samples (Licandro et al. 2007). (3200) Phaethon’s orbit also brings it extremely close to the Sun, giving it an unusually small perihelion distance (\( \sim 0.14 \) AU).

These atypical characteristics justify detailed study of (3200) Phaethon as it could be some form of rare transition object (e.g., an extinct/dormant comet or previously volatile-rich asteroid) that can provide insights into how minor bodies evolve. The combination of its size (\( \sim 5.10 \) km), albedo (\( \sim 0.11 \)), and near-Earth orbit also allows (3200) Phaethon to periodically appear quite bright from Earth (\( \sim 15 \) mag), permitting very precise ground-based observations. Thus we have collected an extensive time series photometry data set for (3200) Phaethon and employed a light curve inversion technique (Kaasalainen et al. 2001; Kaasalainen & Torppa 2001) to refine the object’s rotational period and pole orientation as well as derive a shape model. We focus on these key physical properties as they have important consequences for an object’s origin and history (e.g., La Spina et al. 2004) as well as its thermophysical properties (e.g., Ohtsuka et al. 2009).

We begin in Section 2 by presenting the observations, data reduction, and time series photometry that resulted in 16 light curves spanning almost two decades. In Section 3, we use this unprecedentedly large data set for (3200) Phaethon to refine the object’s rotational period as well as to derive a highly oblique rotational pole with a negative ecliptic latitude. In Section 4, we discuss the implications of our findings, namely, support for previous evidence of an origin in the inner main asteroid belt as well as the potential for deeply buried volatiles fueling impulsive yet rare cometary outbursts. We conclude in Section 5 with suggestions for future work to further investigate these possible scenarios.

2. OBSERVATIONS, REDUCTION, AND PHOTOMETRY

2.1. Observations

We obtained time series photometry over 15 nights from 1994 to 2013. These observations are summarized in Table 1. All but three nights used the Tektronix 2048 × 2048 pixel CCD camera on the University of Hawaii 2.2 m telescope on Mauna Kea. Two nights used the PRISM 2048 × 2048 pixel CCD camera on the Perkins 72 inch telescope at the Lowell Observatory in Flagstaff, Arizona, while one night used the Optic 2048 × 4096 CCD camera also on the University of Hawaii 2.2 m telescope. All observations used the standard Kron–Cousins \( R \) filter with the telescope guiding on (3200) Phaethon at non-sidereal rates.

2.2. Reduction and Photometry

Raw images were processed with standard IRAF routines for bias subtraction, flat-fielding, and cosmic ray removal.
We performed photometry using the IRAF phot routine with circular apertures typically 5" in radius, although aperture sizes changed depending on the night and/or exposure as they were chosen to consistently include 99.5% of the object’s light. Sky subtraction used either an annulus around the photometry aperture or median-combined samples of nearby patches of clear sky. (3200) Phaethon appeared point-like in all images, justifying our use of aperture photometry.

For photometric nights, we calibrated instrumental magnitudes using standard stars from Landolt (1992). The standard stars ranged sufficiently in color and air mass to correct for color terms and extinction, thereby providing absolute flux calibrations; we computed transformations between the Kron–Cousins and SDSS filters using equations provided on the SDSS website.

Unfortunately, SDSS did not cover the star fields of our 2004 November and 2013 December observing runs. For these nights, we used the weighted mean magnitude of each field star across stable periods (or over the entire night, if no period was sufficiently stable) as our reference magnitudes when performing differential photometry. These light curves should therefore be considered relative rather than absolute. This approach was sufficient for the purposes of our analysis as the light curve inversion technique employed in this work can accommodate relative light curves.

### 2.3. Light Curves

Our observations resulted in 16 light curves, as shown in Figure 1. Note that one night (2004 November 21) contained two full light curves, thus 15 nights of observations resulted in 16 full or partial light curves. The supplementary online information contains a table of Julian Date (JD), Universal Time (UT), and $R$ magnitude for each light curve point in our data set. The light curves span many distinct viewing geometries (i.e., different combinations of ecliptic longitude and latitude) over roughly 20 years. On average, they cover ∼75% of a full rotation period with ∼33 photometry points. Their asymmetric double peaks and significant changes in shape and amplitude over time are probably due to a combination of changing viewing geometries as well as (3200) Phaethon’s high orbital inclination relative to the ecliptic (∼22°) and its potentially non-spherical shape (see Figure 6).

### 2.4. Phase Curve

Our data set spans a wide range of phase angles ($\alpha$), allowing us to construct a phase curve for (3200) Phaethon. For each night with absolute calibrations, we calculated the reduced $R$ magnitude using the standard equation:

$$ H(\alpha) = m(\alpha)_R - 5 \log(R\Delta), $$

(1)

where $m(\alpha)_R$ is the weighted mean of the observed $R$ magnitudes at a given $\alpha$, and $R$ and $\Delta$ are the associated heliocentric and geocentric distances in AU, respectively. As shown in Figure 2, our data set only covers the linear portion of (3200) Phaethon’s phase curve. Thus we could strongly constrain $G$ (the slope parameter), but not $H$ (the absolute magnitude), as observations at small phase angles are important for constraining the upturn of the model phase function when using the $HG$ formalism (Bowell et al. 1989). We minimized the residuals between the data and...
the model phase function, resulting in best-fit model parameters of $H = 13.90$ and $G = 0.06$. This low value of $G$ is consistent with C-type asteroids, which have typical $G$ values of $0.05 \pm 0.02$ (compared to S-type asteroids with typical $G$ values of $0.23 \pm 0.02$; Lagerkvist & Magnusson 1990). This agrees with (3200) Phaethon’s classification as an F-type (Tholen 1985) or B-type (Green et al. 1985) asteroid, both subtypes of C-type asteroids.

3. PERIOD, POLE ORIENTATION, AND SHAPE MODEL

3.1. Light Curve Inversion

Light curve inversion is used to derive rotational states and shape models from disk-integrated, time series photometry. Light curves represent the instantaneous scattered sunlight received at Earth from the projected surface area of a rotating asteroid.
object. The projected surface changes with viewing geometry, affecting the observed light curve amplitude and shape. With data at a sufficient number of different viewing geometries (i.e., different combinations of ecliptic longitude and latitude), it is possible to reconstruct the unprojected shape of the object and solve for its rotational state.

We used the light curve inversion software convexinv to refine the rotational period and pole orientation of (3200) Phaethon as well as determine its shape. Convexinv uses the light curve inversion scheme described in Kaasalainen et al. (2001) and Kaasalainen & Torppa (2001) to compute the light curve inversion scheme described in Kaasalainen et al. (2001) and Kaasalainen & Torppa (2001) to compute a shape–spin–scattering model that gives the best fit to a set of input light curves. The software is available online at the Database of Asteroid Models from Inversion Techniques (DAMIT; Durech et al. 2010).9

### 3.2. Rotational Period

Previous estimates of (3200) Phaethon’s rotational period used only two to three light curves and showed significant spread, from 3.57 ± 0.02 hr (Pravec et al. 1998) to 3.604 ± 0.001 hr (Meech et al. 1996). We therefore refined (3200) Phaethon’s rotational period by inputting our data set into the period_scan program (part of the convexinv package). Period_scan searches a user-specified period interval to find the best-fit model to the input light curve, as defined by a minimum relative \( \chi^2 \) value (\( \chi^2_{\text{Rel}} \); see convexinv documentation for details).

We first scanned 1.0–10.0 hr to confirm the global \( \chi^2_{\text{Rel}} \) minimum near \( \sim 3.6 \) hr, then scanned 3.595–3.610 hr at intervals of \( 3 \times 10^{-5} \) hr to refine this period; Figure 3 shows the resulting \( \chi^2_{\text{Rel}} \) minimization plot. Because period_scan does not take into account observational errors, we determined the best-fit period and associated error using a Monte Carlo approach. We added random Gaussian-distributed noise scaled to typical photometry errors (\( \sim 0.01 \) mag) to each light curve point, then used period_scan to find the period associated with the minimum \( \chi^2_{\text{Rel}} \) value. We repeated this 100 times, taking the mean and standard deviation of the results as our final period estimate, \( P = 3.6032 \pm 0.0008 \) hr.

### 3.3. Pole Orientation

To derive pole solutions convexinv requires a set of light curves, an estimated rotational period, and an initial guess of pole orientation. Given these inputs the program performs a user-specified number of iterations until converging on a best-fit pole solution defined by a minimum \( \chi^2_{\text{Rel}} \) value. To find our best-fit pole solution given our uncertainties on (3200) Phaethon’s rotational period, we performed 160 “runs” where each run used a unique period (covering the range found in Section 3.2 with a resolution of \( 1 \times 10^{-5} \) hr) and tested a grid of 156 initial pole guesses (equally spaced in ecliptic coordinate space). We took the best-fit solution from each run as that associated with the minimum \( \chi^2_{\text{Rel}} \) value. The best-fit results from each of these 160 runs are shown in Figure 4 (for ecliptic latitude) and Figure 5 (for ecliptic longitude); there is clear clustering of best-fit results at \( \beta \sim -20^\circ \) and \( \lambda \sim +90^\circ \). We determined our final pole solution by taking the mean and standard deviation of the results within 10% of the lowest \( \chi^2_{\text{Rel}} \) value across all runs (in order to filter out poor fits). We also omitted solutions more than \( \pm 90^\circ \) from \( \lambda \sim +90^\circ \) in order to avoid contamination from possible mirror solutions (due to the 180° degeneracy in \( \lambda \) that is common when using light curve inversion to derive rotational pole orientations). This gave a final pole solution of \( \lambda = +85^\circ \pm 13^\circ \) and \( \beta = -20^\circ \pm 10^\circ \).

Our results confirm one of the preliminary pole solutions found by Krugly et al. (2002), namely, \( \lambda_1 = 97^\circ \pm 15^\circ \) and \( \beta_1 = -11^\circ \pm 15^\circ \). Thus (3200) Phaethon appears to have a highly oblique rotational pole. Obliquity is the angle between an object’s rotational pole and the normal to its orbital plane, where high obliquity refers to a pole oriented very close to the orbital plane. (3200) Phaethon’s high orbital inclination of \( i \approx 22^\circ \) relative to the ecliptic, combined with its longitude of ascending node at \( \Omega \approx 256^\circ \), means that the rotational pole derived above could be only \( \sim 2^\circ \) above its orbital plane, corresponding to a notably high obliquity of \( \sim 88^\circ \).

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9 [http://astro.troja.mff.cuni.cz/projects/asteroids3D/web.php](http://astro.troja.mff.cuni.cz/projects/asteroids3D/web.php)
3.4. Shape Model

*Convexi* uses a set of input light curves and a user-defined rotation period and pole orientation to derive a shape model in the form of a convex polyhedron described by a set of triangular facets and vertices (Kaasalainen & Torppa 2001). Prior to this work, a shape model for (3200) Phaethon had not been attempted because of insufficient data and thus uncertain period and pole estimates. Figure 6 presents our shape model for (3200) Phaethon using the rotational period and pole orientation derived above; the axis ratios are $x/y \approx 1.04$ and $x/z \approx 1.14$. We performed a sensitivity analysis by testing period and pole solutions randomly perturbed by our estimated errors. We found that in some cases 3200 Phaethon was predicted to be a long-axis rotator (i.e., $x/z < 1$). This is an interesting result, as long-axis rotation indicates a perturbed state (e.g., Samarasinha et al. 2004). However, when visually comparing the model results to the data, our best-fit solutions gave a substantially better fit to the data (see Figure 1) than the perturbed solutions.

4. DISCUSSION

4.1. Preferential Heating at Perihelion

Ohtsuka et al. (2009) performed a detailed thermal analysis of (3200) Phaethon using the preliminary rotational pole initially found by Krugly et al. (2002) and confirmed in this work. They found that (3200) Phaethon’s highly oblique rotational pole, combined with its highly inclined and eccentric orbit, causes preferential heating of its northern hemisphere at perihelion. This is illustrated in Figure 7 (to be compared to Figure 1(b) in Ohtsuka et al. 2009), which shows (3200) Phaethon’s sub-solar latitude as a function of true anomaly. When (3200) Phaethon is at perihelion (i.e., only 0.14 AU from the Sun) its northern hemisphere appears to be exposed to intense heating.

Ohtsuka et al. (2009) also calculated (3200) Phaethon’s sub-solar equilibrium surface temperature as a function of its orbit (see their Figure 2). They found that at perihelion solar-radiation heating causes the surface temperature of (3200) Phaethon to exceed 800 K, sufficient to decompose and dehydrate minerals such as serpentine phyllosilicates. Ohtsuka et al. (2009) hypothesized that this could result in latitude-dependent color variations on the surface of (3200) Phaethon. Preferential heating would thermally metamorphose and dehydrate phyllosilicates in the more exposed areas, altering the mineralogy to create a visibly bluer surface in the northern hemisphere. They then used previously published spectra to test whether (3200) Phaethon’s spectral gradient became more negative (i.e., bluer) at a bluer surface at northern latitudes, they were ultimately inconclusive.

We therefore searched for color variation as a function of sub-Earth latitude using nights from our data set that contained multi-filter (BVR) photometry supplemented with literature color values (see Table 2). Although none of these observations cover positive sub-Earth latitudes, the northern hemisphere should be increasingly visible for sub-Earth points $> -45^\circ$. We calculated our $B-V$ and $V-R$ colors by interpolating our $R$ magnitudes to the UT times of the other filter measurements, using propagation of errors for subtraction to estimate uncertainties. Due to the fine time sampling of our $R$-band data (typically $\leq 2$ minutes), uncertainties on the interpolated magnitudes are probably not larger than for the individual measurements. As shown in Table 2, we found that $B-V$ color for (3200) Phaethon does
Figure 6. Shape model of (3200) Phaethon derived using our best-fit period and pole solutions. The model is shown in three orthogonal views: the left and center panels show equatorial views that are 90° apart (pole oriented upward) while the right panel shows a pole-on view (pole oriented out of the page). The axis ratios are \(x/y \approx 1.04\) and \(x/z \approx 1.14\).

Figure 7. Variations in sub-solar latitude along (3200) Phaethon’s orbit. The star indicates perihelion, when the sub-solar point on (3200) Phaethon is at \(\sim 44°\) latitude. The solid line shows the sub-solar latitude when using the pole orientation derived in this work. The dotted line shows the sub-solar latitude when using the pole orientation derived by Krugly et al. (2002) and used in the thermal analysis of Ohtsuka et al. (2009). Both indicate that (3200) Phaethon experiences preferential heating of its northern hemisphere at perihelion.

decrease (become bluer) as the sub-Earth point approaches the northern hemisphere. Although \(V-R\) color does not show a clear trend, these filters sample redder wavelengths. These results therefore support Ohtsuka et al. (2009)’s prediction of preferential thermal processing in the northern hemisphere of (3200) Phaethon at perihelion.

It is important to note that the color variation predicted by Ohtsuka et al. (2009) requires that the preferential heating of the present planetary epoch be the primary metamorphic heat source of (3200) Phaethon. In other words, (3200) Phaethon could not have been heated to more than a few hundred degrees prior to being injected into its current near-Sun orbit roughly \(\sim 10^3\) yr ago (corresponding to the age of the Geminids; Gustafson 1989; Ryabova 2007). This is plausible as (3200) Phaethon is classified as an F- or B-type asteroid; these asteroids have been associated with CI/CM carbonaceous chondrites (Hiroi et al. 1996), which are believed to have undergone only moderate heating that can lead to aqueous alteration but not thermal metamorphism.

4.2. Volatile Survival

The evidence for preferential heating of (3200) Phaethon’s northern hemisphere at perihelion, discussed above, raises the possibility of deeply buried volatiles surviving despite an extremely close approach to the Sun. Although a previous calculation of (3200) Phaethon’s core temperature at \(\sim 250\) K (Hsieh & Jewitt 2005) is too high for water ice to survive, this estimate assumed thermal equilibrium. Extreme pole orientations, such as the one found in this work, may allow cooler core temperatures because thermal equilibrium would no longer apply. Boice et al. (2013) performed a more detailed three-dimensional “physico-chemical” modeling of (3200) Phaethon using a highly oblique pole similar to the one found in this work in order to assess whether water ice could still exist in the core of (3200) Phaethon. They found that (3200) Phaethon is likely to contain relatively pristine volatiles in its interior despite repeated close approaches to the Sun, leaving open the possibility of impulsive outbursts as deeply buried volatiles break through the volatile-depleted surface layers. Thus previous failed attempts to detect comet-like activity on (3200) Phaethon (Hsieh & Jewitt 2005; Wiegert et al. 2008) may have been unsuccessful simply because the observations did not coincide with an outburst.

Although very small amounts of activity at perihelion have been observed in (3200) Phaethon using the space-based STEREO solar observatory, this activity was interpreted to arise from thermal fracture and desiccation cracking due to intense heating at perihelion, rather than comet-like activity from deeply buried volatiles (Jewitt & Li 2010). Moreover, the mass loss rate from the short-lived dust tails at perihelion is insufficient to account for ongoing replenishment of the Geminid stream, and the dust particles may also be gravitationally unbound to the solar system, preventing them from contributing to the Geminids (Jewitt et al. 2013).

4.3. Main Belt Origin

(3200) Phaethon has been linked to the main asteroid belt in previous dynamical and compositional studies. Bottke et al. (2002a) used dynamical modeling of (3200) Phaethon’s orbit to show that it has a zero probability of originating from comet reservoirs such as the Jupiter Family Comet region, but a 50% and 80% probability of originating from the central and inner main asteroid belt, respectively. de León et al. (2010) then made the compositional link by showing significant similarities
between the reflectance spectra of (3200) Phaethon and another B-type asteroid in the central main belt, 2 Pallas.

The negative ecliptic latitude of (3200) Phaethon’s pole derived in this work supports its origin in the inner main asteroid belt. Objects in near-Earth space have a distinct excess of retrograde spins (Kryszczyńska et al. 2007), which has been postulated to result from the dynamical mechanism that transfers objects from the inner main asteroid belt into near-Earth space—namely, the highly efficient $v_6$ resonance. Because the $v_6$ resonance is located at the inner edge of the main belt, it can only be reached by asteroids with orbits evolving inward toward the Sun. The Yarkovsky effect is the well-known mechanism that alters the orbital semimajor axes of asteroids (see Bottke et al. 2002b for an overview of the influence of the Yarkovsky effect on the dynamical evolution of asteroids); however, the Yarkovsky effect only evolves orbits inward for asteroids with retrograde rotations (i.e., $\beta < 0$). Therefore, the observed excess of retrograde spins among near-Earth objects has been explained by “dynamical filtering” when retrograde main belt asteroids evolving inward due to the Yarkovsky effect are preferentially ejected into near-Earth space via the $v_6$ resonance (La Spina et al. 2004).

It is important to note that the Yarkovsky effect is less efficient for objects with highly oblique poles, such as (3200) Phaethon. Therefore, we must consider alternative mechanisms for altering (3200) Phaethon’s rotational pole to such an extreme orientation while in near-Earth orbit. Collisions can alter rotational pole orientations, although they are highly improbable for an object like (3200) Phaethon due to its small size and the limited population of potential impactors in the inner solar system. The Yarkovsky–O’Keefe–Radzievskii–Pattack (YORP) effect can also affect spin states, however timescales for changing obliquity by $\sim 90^\circ$ are typically million years (Rubincam 2000); given the young age of the Geminids ($\sim 10^3$ yr; Gustafson 1989; Ryabova 2007), it is unlikely that there has been sufficient time for the YORP effect to significantly alter (3200) Phaethon’s rotational state. However, if (3200) Phaethon is indeed still active, variable outbursts may potentially explain the object’s extreme pole orientation.

5. SUMMARY AND FUTURE WORK

We have used an extensive time series photometry data set, consisting of 16 light curves spanning roughly 20 years, to refine (3200) Phaethon’s rotational period and pole orientation as well as derive its shape model. We find a period of $P = 3.6032 \pm 0.0008$ hr with a pole orientation of $\lambda = +85^\circ \pm 13^\circ$ and $\beta = -20^\circ \pm 10^\circ$. Key areas of future work include confirming surface color variation due to preferential heating at perihelion (e.g., by measuring $B-V$ and $V-R$ colors at positive sub-Earth latitudes) and continuing the search for low-level cometary outbursts (e.g., by serendipitous observation).

Another important area of future work will be deriving pole solutions for the two smaller minor bodies associated with (3200) Phaethon—2005 UD (Jewitt & Hsieh 2006) and 1999 YC (Ohtsuka et al. 2008)—in order to assess their possible formation mechanisms. If all three bodies have randomized pole orientations, this may point to their formation via explosive activity in (3200) Phaethon soon after it was transferred to its current near-Sun orbit from the main belt. Suddenly exposing a volatile-rich (3200) Phaethon to intense heating at perihelion could have resulted in a burst of activity that formed the Geminids as well as 2005 UD and 1999 YC, leaving (3200) Phaethon dormant/extinct. This is an enticing interpretation given that the Geminids is a dynamically young meteor stream, which suggests ongoing activity, yet (3200) Phaethon has exhibited no known comet-like outbursts sufficient to replenish the stream. Simultaneous formation of the Geminids, 2005 UD, and 1999 YC with extinction/dormancy of (3200) Phaethon would account for both the youth of the Geminids as well as the lack of activity seen in (3200) Phaethon. However because such an event could significantly alter rotational states, the negative ecliptic latitude of (3200) Phaethon’s pole would no longer be evidence for its origin in the inner main belt (although this would not preclude a possible origin in the main belt).

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REFERENCES

Boice, D. C., Benkhoff, J., & Huebner, W. F. 2013, BAAS, 45, 413.32
Bottke, W. F., Morbidelli, A., Jedicke, R., et al. 2002a, Icar, 156, 399
Bottke, W. F., Jr., Vokrouhlický, D., Rubincam, D. P., & Broz, M. 2002b, Asteroids III, 395
Bowell, E., Hapke, B., Domínguez, D., et al. 1989, in Asteroids II, ed. R. P. Binzel, T. Gehrels, & M. S. Matthews (Tucson, AZ: Univ. Arizona Press), 524
de León, J., Campins, H., Tsiganis, K., Morbidelli, A., & Licandro, J. 2010, A&A, 513, A26
Dundon, L. 2005, M.S. thesis, Univ. Hawaii
Durech, J., Sidorin, V., & Kaasalainen, M. 2010, A&A, 513, A46
Green, S. F., Meadows, A. J., & Davies, J. K. 1985, MNRS, 214, 29P
Gustafson, B. A. S. 1989, A&A, 225, 533
Hiroi, T., Zolensky, M. E., Pieters, C. M., & Lipschutz, M. E. 1996, M&PS, 31, 321
Hsieh, H. H., & Jewitt, D. 2005, ApJ, 624, 1093
Jewitt, D. 2013, AJ, 145, 133
Jewitt, D., & Hsieh, H. 2006, AJ, 132, 1624
Jewitt, D., & Li, J. 2010, AJ, 140, 1519
Jewitt, D., Li, J., & Agarwal, J. 2013, ApJL, 771, L36
Kaasalainen, M., & Torppa, J. 2001, Icar, 153, 24
Kaasalainen, M., Torppa, J., & Mainonen, K. 2001, Icar, 153, 37
Kasuga, T., & Jewitt, D. 2008, AJ, 136, 881
Krugly, Y. N., Belskaya, I. N., Shevchenko, V. G., et al. 2002, Icar, 158, 294
Kryszczyńska, A., La Spina, A., Paolicchi, P., et al. 2007, Icar, 192, 223
La Spina, A., Paolicchi, P., Kryszczyńska, A., & Pravec, P. 2004, Natur, 428, 400
Lagerkvist, C.-I., & Magnusson, P. 1990, A&AS, 86, 119
Laun, P. L., Toth, I., Fernández, Y. R., & Weaver, H. A. 2004, in Comets II, ed. M. C. Festou, H. U. Keller, & H. A. Weaver (Tucson, AZ: University of Arizona Press), 223
Landolt, A. U. 1992, AJ, 104, 304
Licandro, J., Campins, H., Mothé-Diniz, T., Pinilla-Alonso, N., & de León, J. 2007, A&A, 461, 751
Meach, K. J., Hainaut, O. R., & Buie, M. W. 1996, Abstracts of ACM 1996, 42 Ohtsuka, K., Arakida, H., Ito, T., Yoshikawa, M., & Asher, D. J. 2008, M&PS, 43, 5055
Ohtsuka, K., Nakato, A., Nakamura, T., et al. 2009, PASJ, 61, 1375
Pravec, P., Wolf, M., & Šarounová, L. 1998, Icar, 136, 124
Rubincam, D. P. 2000, Icar, 148, 2
Ryabova, G. O. 2007, MNRAS, 375, 1371
Samarasinha, N. H., Mueller, B. E. A., Belton, M. J. S., & Jorda, L. 2004, in Comets II, ed. M. C. Festou, H. U. Keller, & H. A. Weaver (Tucson, AZ: Univ. Arizona Press), 281
Tholen, D. J. 1985, IAU Circ., 4034, 2
Tody, D. 1986, Proc. SPIE, 627, 733
Whipple, F. L. 1983, IAU Circ., 3881, 1
Wiegert, P. A., Houle, M., & Peng, R. 2008, Icar, 194, 843
Williams, I. P., & Wu, Z. 1993, MNRAS, 262, 231
York, D. G., Adelman, J., Anderson, J. E., Jr., et al. 2000, AJ, 120, 1579