SURFACE DETONATIONS IN DOUBLE DEGENERATE BINARY SYSTEMS TRIGGERED BY ACCRETION STREAM INSTABILITIES

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ABSTRACT

We present three-dimensional simulations on a new mechanism for the detonation of a sub-Chandrasekhar CO white dwarf in a dynamically unstable system where the secondary is either a pure He white dwarf or an He/CO hybrid. For dynamically unstable systems where the accretion stream directly impacts the surface of the primary, the final tens of orbits can have mass accretion rates that range from $10^{-5}$ to $10^{-3} \ M_\odot \ s^{-1}$, leading to the rapid accumulation of helium on the surface of the primary. After $\sim 10^{-2} \ M_\odot$ of helium has been accreted, the ram pressure of the hot helium torus can deflect the accretion stream such that the stream no longer directly impacts the surface. The velocity difference between the stream and the torus produces shearing which seeds large-scale Kelvin–Helmholtz instabilities along the interface between the two regions. These instabilities eventually grow into dense knots of material that periodically strike the surface of the primary, adiabatically compressing the underlying helium torus. If the temperature of the compressed material is raised above a critical temperature, the timescale for triple-$\alpha$ reactions becomes comparable to the dynamical timescale, leading to the detonation of the primary’s helium envelope. This detonation drives shock waves into the primary which tend to concentrate at one or more focal points within the primary’s CO core. If a relatively small amount of mass is raised above a critical temperature and density at these focal points, the CO core may itself be detonated.

Key words: accretion, accretion disks – binaries: general – instabilities – novae, cataclysmic variables – supernovae: general – white dwarfs

Online-only material: color figures

1. INTRODUCTION

White dwarfs (WDs), the end point of stellar evolution for most stars, are extremely common, with about $10^{10}$ of them residing within the Milky Way (Napiwotzki 2009). WDs are frequently observed in binary systems with normal stellar companions, and, less frequently, with compact stellar companions. Double degenerate (DD) systems are those in which the companion is another WD. Typically, DD systems are formed via common envelope evolution (Nelemans et al. 2001). If, the final result of this evolutionary process is a binary consisting of a carbon–oxygen (CO) WD and a lower-mass helium WD companion (Napiwotzki et al. 2007).

For decades, Type Ia supernovae (SNe) have been employed as standard candles. Still, even the preferred mechanism exhibits substantial variability (Timmes et al. 2003; Kasen et al. 2009). Complicating this issue further is that WDs may not need to have masses near the Chandrasekhar limit to be capable of exploding; other mechanisms include collisions between WDs in dense stellar environments such as the cores of globular clusters (Rosswog et al. 2009a), tidal encounters with moderately massive black holes (Rosswog et al. 2008, 2009b; Ramirez-Ruiz & Rosswog 2009), or as we are introducing in this Letter, the accretion of dense material from an He WD companion.

At the distance of tens of WD radii, gravitational radiation can bring two WDs close enough for the less-massive WD (secondary) to overfill its Roche lobe and begin transferring mass to the more-massive WD (primary). Because of the mass–radius relationship of WDs, mass transfer is often unstable and can eventually lead to a merger (Marsh et al. 2004; Gokhale et al. 2007). For binary mass ratios close to unity the circularization radius $R_0$ drops below the radius of the primary $R_1$, and thus the accretion stream will directly impact the primary’s surface.

Most studies of dynamically unstable DD systems focus on the evolution of the post-merger object and, assuming that the final object has a mass larger than the Chandrasekhar limit, on how the merged remnant may eventually lead to a Type Ia SN (Livio 2000; Yoon et al. 2007). These models all assume that the rapid accretion that precedes coalescence is uneventful. In this Letter, we present three-dimensional hydrodynamics simulations that demonstrate that explosive phenomena are a likely consequence of the high accretion rates characteristic of the final stages of a merger in a DD system. In some cases, these explosive phenomena may lead to the complete detonation of the CO primary.

2. NUMERICAL METHOD AND INITIAL MODELS

The lead-up to the merger has only been studied recently due to the sensitivity of the accretion to the transfer of angular momentum. Several groups have simulated these mergers in three dimensions using particle-based codes (Benz et al. 1990; Rasio & Shapiro 1995; Segretain et al. 1997; Guerrero et al. 2004; Dan et al. 2009), with the latter being able to resolve the final $\sim 100$ orbits of the binary prior to coalescence. Smoothed particle hydrodynamics (SPH) simulations, with their excellent angular momentum conservation, are well suited to determine the binary orbital evolution. However, because the SPH particles have a fixed mass and typical accretion rates are $\gtrsim 10^{-5}$ the total mass of the system per orbit, the accretion stream is only resolved by hundreds of particles at best. Consequently, SPH approaches are unable to resolve any of the accretion stream’s detailed structure, including how the stream impacts the surface of the primary.
Eulerian codes are able to provide high resolution based on any combination of local and global simulation properties, and thus are ideal for systems where the regions of interest do not overlap with the regions of highest density (New & Tohline 1997; Swesty et al. 2000). Unfortunately, it is difficult to accurately simulate the overall orbital evolution for many orbits in grid-based codes due to the non-conservation of angular momentum (Krumholz et al. 2004), although a careful choice of coordinate system has led to recent success (D’Souza et al. 2006; Motl et al. 2007). Because the stability of the system depends on the structure of the primary and the secondary, the grid-based simulations that investigate stability must fully resolve both stars, and thus the stream and the primary’s surface are less resolved in these simulations.

Here we follow a hybrid approach that combines the strengths of both SPH- and grid-based methods. We follow the impact of the mass transfer onto the orbital evolution by performing an SPH simulation (M. Dan et al. 2010, in preparation) and use the obtained, time-dependent results for orbital separation and $M$ as boundary conditions for FLASH (Fryxell et al. 2000). This combination allows us to realistically determine the dynamic stability of the binary while not sacrificing our spatial resolution of the accretion.

In FLASH, the primary is built under the assumption of spherical hydrostatic equilibrium and a constant temperature of $5 \times 10^5$ K, and is mapped into the simulation explicitly. The secondary is not mapped directly into the grid and is taken to be a point mass surrounded by a spherical outflow boundary condition. The simulation is performed in a non-inertial frame rotating with angular frequency $\omega = \sqrt{G(M_1 + M_2)/a^3}$ about the barycenter. The primary’s gravity is calculated using a multipole expansion of its potential, and because the quadrupolar contribution of the secondary is negligible, we approximate the secondary’s gravitational field as a monopole. Because the choice of frame and the presence of the secondary changes the hydrostatic configuration of the primary, we first allow the primary to slowly relax in the presence of the secondary’s potential by removing a fraction of its kinetic energy every time step over many dynamical timescales.

The nuclear composition of the fluid is evolved via the 13 element $\alpha$-chain network of Timmes (1999). Pressures and temperatures are calculated using the Helmholtz equation of state (Timmes & Swesty 2000). The accretion rate provided by the SPH calculation is used to generate a quasi-hydrostatic inflow boundary condition to replicate the flow of matter from the secondary to the primary (Figure 1). The boundary we use is cone-shaped with the apex located at $L_1$, and mass is added to the cone under the assumption that the stream is in hydrostatic equilibrium in the direction perpendicular to the barycentric line (Lubow & Shu 1976). The flow is directed toward the barycenter of the system at velocity $v = c_s \sim 10^8$ cm s$^{-1}$, the sound speed within the secondary. In all simulations presented here, the stream is assumed to be pure He. The four simulations that we have performed are summarized in Table 1.

### 3. ACCRETION STREAM INSTABILITIES

In a binary system undergoing mass transfer, the fate of the accretion stream is determined by ratio $R_1/R_b$. For all three of the binaries we describe $R_b < R_1$ and thus the stream would directly impact the surface of the primary assuming the stream was collisionless. However, the stream can eventually be deflected by the ram pressure of the thick torus of helium that gradually accumulates on the primary’s surface, preventing a direct impact.

As the sound speed within the torus is far smaller than the Keplerian rotation velocity, the collision between the torus and the stream is highly supersonic ($M > 10$), which leads to the development of a standing shock (Figure 1, region I). This shock establishes pressure equilibrium across the stream–torus interface. Because of the temperature increase of the material falling from $L_1$ to the surface of the primary, the torus consists of material heated to a temperature close to the virial temperature of $GM_1m_p/R_bk_b \sim 10^8$ K. Radiation...
pressure becomes competitive with degeneracy pressure at these temperatures and densities, and as a result the torus has a density smaller than the incoming accretion stream.

Because the accretion stream and the helium torus do not move in the same direction, the difference in velocity at the interface is substantial, $U_1 - U_2 \sim \sqrt{GM_1/r_1 \sqrt{2 - \cos \theta}}$, where $\theta$ is the angle between the stream and torus velocities. This shear can lead to the rapid growth of Kelvin–Helmholtz instabilities along the interface between the two regions (Figure 1, region II). An important factor in determining which perturbations are unstable is the magnitude of the restoring force perpendicular to this interface. The acceleration $g$ limits the instability to $k > k_{\text{min}}$ (Chandrasekhar 1961)

$$k_{\text{min}} = \frac{g(\alpha_1 - \alpha_2)}{\alpha_1 \alpha_2 (U_1 - U_2)^2},$$

(1)

where $\alpha_1 \equiv \rho_1/(\rho_1 + \rho_2)$ and $\alpha_2 \equiv \rho_2/(\rho_1 + \rho_2)$. As long as $g > 0$, only perturbations with wavelength $\lambda < \lambda_{\text{max}} = 2\pi/k_{\text{min}}$ can grow. Within the primary’s Roche lobe, $g$ is determined by the combination of the primary’s gravity and the Coriolis force

$$g = 2\Omega|\vec{v}| - \frac{GM_1 |\vec{v}| \times \vec{v}}{|\vec{v}|^2} |\vec{v}|.$$  

(2)

Because the Coriolis force is always perpendicular to the velocity, its contribution to $g$ is always equal to the magnitude of the force. Only the component of the primary’s gravity that is perpendicular to $\vec{v}$ will contribute to $g$. Near $L_1$ where the cumulative gravitational forces are parallel to the velocity, the Coriolis term is dominant and is directed away from the primary, and thus $g$ is positive. As the stream falls toward the surface of the primary, $U_1 - U_2$ continually increases, allowing progressively longer wavelengths to become unstable. And because the Coriolis effect is $\propto |\vec{v}| \propto |\vec{v}|^{-1/2}$ while the primary’s gravity is $\propto |\vec{v}|^{-2}$, the primary’s gravity eventually becomes the dominant contributor to the restoring force. As the primary’s gravity is opposite to the Coriolis force, $g$ eventually changes sign, at which point all wave modes become unstable (Figure 1, region III).

The helium torus, which is both clumpy and has a radial density profile, drives the seed vertical displacements in the accretion stream. The torus is highly turbulent, with the largest bulk motions being driven at scales comparable to the width of the accretion stream ($\sim 10^8$ cm) and at speeds that are highly supersonic. Therefore, the power spectrum of the resulting turbulent cascade is given by Burgers turbulence ($E \propto k^{-2}$).

Consequently, perturbations with large wavelengths are seeded with large initial amplitudes, giving them a head start over smaller perturbations. Additionally, power is transferred from large $k$ to small $k$ by the tidal stretching of waves as they fall in the primary’s gravity. A numerical calculation of the growth rate shows that the largest unstable modes experience a 10-fold increase in amplitude in the time it takes to fall from $L_1$ to the primary’s surface. Because the flow is three dimensional, instabilities larger than the stream size cannot form, and the end result is that the stream consists of knots of material that are comparable in size to the stream itself (Figure 1).

4. SURFACE DETONATIONS

We find that instabilities in the accretion stream are present in all four runs once the helium torus has acquired enough mass to deflect the stream. The material that is compressed against the surface of the primary by the dense knots formed in the stream can be heated to billions of degrees Kelvin (Figure 1, region IV). At the onset of mass transfer, the density of the stream is too small to heat the underlying material appreciably. This allows $\sim 1\%-15\%$ of a solar mass of helium to accumulate on the surface of the primary. As the density of the accretion stream increases with the decreasing separation between the WDs, the temperature of the compressed layer can exceed the temperature required to explosively ignite helium via the triple-$\alpha$ process. This leads to a gravitationally confined surface detonation that propagates through the helium torus that wraps around the surface of the primary at approximately the Keplerian velocity (Figure 3).

The conditions required for a successful surface detonations are summarized in Figure 2. Only systems that are dynamically unstable will ever have accretion rates capable of igniting surface detonations via stream instabilities, and thus the lowerright region of the figure is excluded. The question of whether the surface detonation will occur in a given binary is tricky to answer because the process is highly stochastic; the impact trajectory, density, and geometry of the knots that initiate the detonations vary considerably over the course of the simulations. Nevertheless, we can estimate when surface detonations will occur by comparing the timescale for triple-$\alpha$ reactions $\tau_{3\alpha}$ (Caughlan & Fowler 1988) to the dynamical timescale $\tau_{\text{dyn}} \approx R_1/v_{\text{esc},1}$ at the surface of the primary.

For a surface detonation to involve a significant amount of mass, the system must accrete material at a rate for which $\tau_{3\alpha} > \tau_{\text{dyn}}$, and then transition to a rate where $\tau_{3\alpha} \lesssim \tau_{\text{dyn}}$. By solving the equations of motion for a test particle released
The density structure of the torus is approximately fixed as the system evolves toward merger because $\phi$ only increases slightly due to mass accretion. Meanwhile the stream density continually increases, resulting in the contour of $\tau_{30} = \tau_{\text{dyn}}$ moving leftwards in Figure 2. When $\tau_{30} \lesssim \tau_{\text{dyn}}$, the increase in temperature of the torus can no longer be controlled by adiabatic expansion, which results in thermonuclear runaway and a detonation in the helium torus.

5. RESULTS AND DISCUSSION

Surface detonations are present in both of the longer runs with a 0.9 $M_\odot$ CO primary, although run B detonates much later in its evolution than run C. The geometry and evolution of the detonations are similar in both runs. A small region of the surface helium is heated to a temperature of $\sim 2 \times 10^9$ K, leading to a detonation front that expands outwards from the ignition site along the primary’s surface. Because the helium layer is toroidal rather than spherical, the front runs out of fuel as it propagates toward the primary’s poles. Consequently, the detonation splits into two fronts that run clockwise and counterclockwise around the equator of the primary. These detonation fronts eventually run into each other along a longitudinal line that is opposite to the original ignition site. The highest temperatures are produced in this convergence region.

For run A, the primary’s surface gravity is too low to compress the helium layer above the critical temperature necessary for thermonuclear runaway. No detonation was observed in run Ba, despite being initialized using a checkpoint from run B just prior to the observed detonation in B. This is because of the stochastic nature of the ignition mechanism—the particular dense knot of material that led to the surface detonation in B has a different shape in Ba, and did not have a favorable geometry for igniting the helium torus. And because Ba has twice the linear resolution...

Figure 2. Hashed region on the lower right shows systems that are definitely dynamically stable, while the sticked region in the upper left shows systems that are definitely unstable. The thick solid line shows the transition from direct impact to disk accretion, while the dot-dashed curve shows the separation between sub- and super-Eddington accretion in the weak coupling limit (Marsh et al. 2004). The contours show where $\tau_{\text{dyn}} = \tau_{30}$ for different stream densities $\rho_{30} = \rho_3/10^5$ assuming a torus density of $3 \times 10^5$ g cm$^{-3}$. Surface detonations are likely for systems that accrete with $\rho_3$ for which $\tau_{\text{dyn}} < \tau_{30}$ and then experience an increase in $\rho_3$ until $\tau_{30} > \tau_{\text{dyn}}$.

Figure 3. Volumetric snapshots showing the temperature $T$ and log $\rho_{He} = \rho X_{He}$ during the explosive event on the surface of the primary in run C. A dense knot of helium that formed through Kelvin–Helmholtz instabilities in the accretion stream is marked by a magenta arrow. The evolution of the surface detonation is described in Section 5.

(A color version of this figure is available in the online journal.)
of run B, we could only afford to evolve it for a short period of time.

If a helium surface detonation occurs as the result of stream instabilities in a DD system, the resulting transient event could dramatically increase the amount of focusing by forcing the shocks to converge at a single point rather than a locus of points. Second, FHR does not use a nuclear network and makes the simplifying assumption that the entire He envelope is burned to Ni, which naturally overestimates the energy injected into the CO core when compared to the more realistic case where burning is incomplete.

Because of these differences, the conditions for double detonation are still not met even in our run with the most favorable shock geometry and strongest surface detonation (run C). In the focusing region of run C, the temperature and density are $2.5 \times 10^8$ K and $2.0 \times 10^7$ g cm$^{-3}$, respectively. Conditions for CO core detonation may be more propitious in systems containing a slightly more massive primary, but ultimately the successful detonation of the core depends on the precise distribution of temperature and density within the high-pressure regions of the convergence zone (Seitenzahl et al. 2009).

The mechanism reported here for the detonation of a sub-Chandrasekhar CO WD in a dynamically unstable binary is not tied to a particular mass scale and therefore allows for considerably more diversity. As outlined above, mass transfer between a pure He WD or an He/CO hybrid and a CO WD before the merger provides a novel pathway to ignite CO WDs. Even if a critical amount of mass is not raised above the conditions required for CO detonation, a peculiar underluminous optical transient should signal the last few orbits of a merging system.

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Figure 4. Maximum temperature $T$ in a mass shell as a function of interior mass $M$ (< $r$) and time for run B. Each shell lies on a surface of equal gravitational potential. The shading is logarithmically binned, with red corresponding to $T_{\text{max}}$ and blue corresponding to $T_{\text{min}} = T_{\text{max}}/10^{1.3}$. The dashed line shows the region where $X_{\text{He}} > 0.02$, while the dotted line shows where $X_{\text{Ne}} > 10^{-3}$. For convenience, we include a zoomed view of the surface detonation as an inset. (A color version of this figure is available in the online journal.)
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