Long-range energy transfer in proteins

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Abstract
Proteins are large and complex molecular machines. In order to perform their function, most of them need energy, e.g. either in the form of a photon, as in the case of the visual pigment rhodopsin, or through the breaking of a chemical bond, as in the presence of adenosine triphosphate (ATP). Such energy, in turn, has to be transmitted to specific locations, often several tens of Å away from where it is initially released. Here we show, within the framework of a coarse-grained nonlinear network model, that energy in a protein can jump from site to site with high yields, covering in many instances remarkably large distances. Following single-site excitations, few specific sites are targeted, systematically within the stiffest regions. Such energy transfers mark the spontaneous formation of a localized mode of nonlinear origin at the destination site, which acts as an efficient energy-accumulating center. Interestingly, yields are found to be optimum for excitation energies in the range of biologically relevant ones.

1. Introduction
Protein dynamics is encoded in their structures and is often critical for their function \cite{1}. Since the early 1980s, it is well known that vibrational non-harmonicity \cite{2, 3} has to be accounted for to understand intra-structure energy redistribution \cite{4–8}. Among nonlinear effects, long-lived, localized modes were suggested to play a key role both by theoretical \cite{9–11} and experimental studies \cite{12–15}. For example, localized vibrations in α-helices have been recently hypothesized to represent a means of concentrating energy during enzymatic catalysis \cite{16, 17}. More generally, persistent motions in hinge regions have been shown to correlate with enzymatic activity by NMR measurements \cite{18}, thus prompting the very idea that some kind of energy storage is required at the pico- to nano-second time scale to regulate functional motions at much longer time scales typical of protein function.

Possible modes of nonlinear origin suggested to influence protein dynamics include topological excitations, such as solitons \cite{19, 20}, as well as Discrete Breathers (DB) \cite{21, 22}. The latter, also known as intrinsic localized modes (ILMs), are spatially localized, time-periodic vibrations found generically in many-body systems as a combined effect of nonlinearity and spatial discreteness \cite{23, 24}. Their existence and stability properties have been widely explored in translationally invariant systems \cite{25} at $T = 0$, and much effort has also been devoted to understanding the role of thermal noise on DBs \cite{26–29}. However, little is known on how DBs are affected by the interplay of spatial heterogeneity and nonlinearity \cite{11, 30, 31}, a fortiori in the context of atomic fluctuations in biological macro-molecules.

A number of general features make discrete breathers appealing candidates for playing a role in energy storage and circulation processes in proteins. Notably, DBs are able to harvest from the background and pin down for long times amounts of energy much larger than $k_BT$. Indeed, their ability to pump energy from neighboring sites is a distinctive signature of DB self-excitation \cite{32}, e.g. observed as a consequence of surface cooling \cite{33–36} or due to modulational instability of band-edge waves in nonlinear lattices \cite{37, 38}. Furthermore, within the frame of a nonlinear network model, we have shown that highly energetic DBs can form easily in proteins \cite{33}, and that they feature strongly site-modulated properties \cite{39}. More precisely, we have shown that spatially localized band-edge normal modes (NM) can be continued from low energies to DB solutions centered at the same sites as the corresponding NMs (the NM sites). Note that the latter lie, as a rule, within the stiffest regions of a protein \cite{33, 39}. More generally, however, DBs display a gap in their excitation spectrum. As a
consequence, they can ‘jump’ to another site as their energy is varied, following spatial selection rules matching the pattern of DBs localized elsewhere [39]. As a matter of fact, such jumps realize efficient *energy transfers*. Hereafter, we show that events of this kind, connecting with high yields even widely separated locations, can be triggered by a localized excitation, so long as its energy $E_0$ lies above a given threshold. Indeed, provided that transfer phenomena of this kind are compatible with cellular constraints, it is tempting to speculate that evolution has found a way to put such long-lived modes at work for lowering energy barriers associated with chemical reactions, e.g. for boosting enzyme efficiency during catalytic processes [40].

2. Methods

Proteins are modeled as networks of nodes of mass $M$ (the $\alpha$-carbons of their amino acid residues) linked by springs. Specifically, in the nonlinear network model (NNM) [33, 39], the potential energy of a protein, $E_p$, has the following form:

$$E_p = \sum_{d_{ij} > R_c} \left[ \frac{k_s}{2} (d_{ij} - d_{ij}^0)^2 + \frac{k_2}{4} (d_{ij} - d_{ij}^0)^4 \right]$$  \hspace{1cm} (1)$$

where $d_{ij}$ is the distance between particles $i$ and $j$, $d_{ij}^0$ their distance in the equilibrium structure (as e.g. solved through x-ray crystallography) and $R_c$ is a distance cutoff that specifies which pairs of nodes are interacting. Note that $k_s = 0$ corresponds to the widely used elastic network model (ENM) [41–43], which has proven useful for quantitatively describing amino acid fluctuations at room temperature [41, 42, 44, 45], as well as for predicting or characterizing large-amplitude functional motions of proteins [46–50] in agreement with all-atom models [51–53], paving the way for numerous applications in structural biology [54–57].

As in previous NNM studies [33, 39], we take $R_c = 10$ Å, $k_s = 5$ kcal/mol/Å$^2$ and fix $k_2$ so that the low-frequency part of the linear spectrum matches actual protein frequencies, as calculated using realistic force fields [54]. When $M = 110$ amu (the average amino acid residue mass), this gives $k_2 = 5$ kcal/mol/Å$^2$. Note that, in view of their coarse-grained nature, network models do not reproduce the high-frequency side of an all-atom linear spectrum. Normal modes in this region correspond to localized motions of chemically bonded atoms that are not included in the model. Moreover, frequencies of these motions are so high (up to $\approx 4000$ cm$^{-1}$ [58, 59]) that, as a consequence of quantum-mechanical effects, most of them are unlikely to be excited at room temperature ($\nu > k_B T / h \approx 200$ cm$^{-1}$). Note also that choosing a given value of $k_s$ amounts to define a typical distance $\ell = \sqrt{k_s/k_2}$ above which nonlinearity starts affecting significantly atomic fluctuations ($\ell = 1$ Å in our case, meaning rather weak anharmonicity). However, it is important to stress that in our dynamical system, energy and $k_s$ are not independent parameters. Therefore, performing an energy-dependent study at fixed $k_s$ or acting vice versa will not yield qualitatively different results. In fact, a simple rescaling of the appropriate units (energies or lengths) would suffice to map ones onto the others.

![Figure 1. Local kicks cause energy pinning through the excitation of discrete breathers. The figure illustrates the formation of a discrete breather at site VAL 177 in subtilisin (PDB code 1AV7), a 274-amino-acid enzyme, following the excitation of the band-edge normal mode (M) or a single-site kinetic energy kick at VAL 177 (R), the residue where the edge NM is centered. The right panel reports the energy $E_b$ found in the nonlinear localized mode as a function of the excitation energy $E_0$. The left panels compare the frequency $\omega$ and the localization index $L$ of the nonlinear mode with those of discrete breather solutions centered at VAL 177 calculated analytically, as described in [39], showing that the nonlinear mode excited after a kick is indeed a discrete breather. The dashed line in the upper-left plot marks the band-edge frequency of the protein network ($\nu_E = 101.6$ cm$^{-1}$).](image)

For each site in a given structure, the maximum-stiffness (MS) direction is computed through the sequential maximum strain algorithm [39]. Following an initial kinetic-energy impulse (kick) at a specific site along the local MS unit vector, a 2 ns microcanonical simulation is performed. After a 1 ns transient period during which a part of the excitation energy flows into the system, the velocity-covariance matrix is computed. Its first eigenvector provides the pattern of correlated site velocities involved in the dominant (most energetic) nonlinear mode (the DB). Accordingly, a transfer is recorded at the site at which this mode is found localized. Projecting the system trajectory on the same eigenvector yields fair estimates of the DB frequency and average energy [33].

The localization index $L$ of a DB centered at site $m$ is obtained from the weight of the latter in the normalized displacement pattern of the DB, namely $L = 100 \times \sum_\alpha \sum_{x,y,z} |\xi_\alpha(m)|^2$, where $\xi_\alpha(m)$ are the components at site $m$ of the corresponding eigenvector.

3. Results

3.1. Discrete breather excitation

Figure 1 summarizes the outcome of one such experiment, where energy is initially either localized in NM (M) or in real (R) space. Typically, the initial excitation is found to spark the formation of a discrete breather, pinning a variable amount of energy $E_b$ at a specific location. When less than 10 kcal mol$^{-1}$ of kinetic energy is injected into the edge NM,
Figure 2. Optimum kick direction for exciting discrete breathers in dimeric citrate synthase (PDB code 1IXE). Percentage of the system energy found in a nonlinear mode as a function of the direction of the initial kick given to SER 213A, the NM site of the band-edge mode. The latter is measured by the angle \( \theta \) between the kick direction and the MS unit vector. In all simulations, the (kinetic) energy of the kick is 55 kcal mol\(^{-1}\) and its direction is chosen at random, except that when the maximum strain (MS) direction is picked instead (black diamond at \( \cos \theta = 1 \)). Filled circles: SER 213A is found to be the most energetic site during the analysis timespan. Stars: it is another one. In one instance, while the kick was given in a direction close to the MS direction (\( \cos \theta = 0.9 \)), the DB jumped on a neighboring site (namely, THR 208A).

nearly all this energy is kept by the DB, whose overlap with the edge NM is large at low energies. Increasing \( E_0 \) further, the frequency of the excited mode detaches from the linear band, while the excitation efficiency \( E_b/E_0 \) is eroded. In fact, as DB localization builds up with energy (see the lower-left panel), the spatial overlap with the edge NM diminishes, thus reducing excitation efficiency [4]. The same DB is also excited when the edge NM site is ‘kicked’ along an appropriate direction, namely the MS one [39] (see data marked (R) in figure 1). In this case, however, the excitation becomes more efficient as \( E_0 \) is increased since the DB asymptotically approaches a single-site vibration. For \( E_0 > 100 \) kcal mol\(^{-1}\), the DB loses its energy, which flows rapidly into the system.

3.2. Directional specificity

We find that the MS direction invariably allows for the most efficient excitation of a nonlinear mode at a given site. Figure 2 illustrates the efficiency of kicks given along the MS direction, with respect to kicks imparted along random directions. The correlation with the squared cosine of the angle between the kick and the MS unit vectors indicates that it is the amount of energy injected along the MS vector which is the dominant factor allowing for efficient excitation of a discrete breather.

Interestingly, kicking away from the MS direction can promote energy transfer to another site. For instance, while a kick along the MS unit vector at the NM site of the band-edge mode invariably results in a DB sitting at the same site, when the direction of the kick is picked at random, discrete breathers localized elsewhere are also observed (see again figure 2). In the following, we take advantage of the fact that MS directions can be easily calculated at any site in any structure [39] in order to investigate energy transfer in a systematic manner.

3.3. Energy transfer

When a given residue is kicked along the MS direction, a transfer event can occur when \( E_0 > \approx 20 \) kcal mol\(^{-1}\) (see an example in figure 3). At peak transfer, more than 75% of such kicks excite a DB localized at the band-edge NM site, while otherwise energy flows toward the NM site of another edge mode. Conversely, when the kick is imparted along a random direction, energy transfer is found to be less efficient.

Quite generally, a transfer event can be observed when almost any site is kicked, and in the majority of cases only a handful of well-defined sites are targeted. This means that energy transfer can occur between widely separated locations. Indeed, as illustrated in figure 4 for myosin, only about 5% of 55 kcal mol\(^{-1}\) kicks result in a DB localized at the same
Figure 4. Energy transfer as a function of distance from the excitation site. The figure illustrates the outcome of an all-site kick experiment in myosin, a large 746-amino-acid enzyme involved in muscle contraction (PDB code 1VOM). The fraction of excitation energy found in the DB is plotted versus the distance (in units of links in the connectivity graph) between the kicked site and the site where the nonlinear mode self-excites. The maximum amount of energy found in the DB decreases with the number of links separating the feed and the target sites. For instance, when GLN 246 is kicked, more than 40% of the energy ends up in a DB localized at ALA 125 (the band-edge NM site). This amounts to four links, corresponding to a span of about 25 Å in real space. Otherwise, when a kick is given to ILE 351 or TYR 34, 25–65% of the excitation energy flows to ALA 125 or LEU 296, the NM site of the third edge normal mode. In cases where more than 30% of the kick energy is transferred away, three sites turn out to be targeted half of the times, namely ALA 125 (27%), LEU 296 (13%) and GLY 451 (7%). When only long-range energy transfers are considered (covering three or more links), the shares raise to 71% and 18% for ALA 125 and LEU 296, respectively. In the remaining cases, the DB is found either at LEU 516 (7%, 14th mode) or at ARG 80 (4%, 10th mode).

In one occurrence, more than 20% of the kick energy ends up in a nonlinear mode localized more than five links away: following a kick at TYR 34, a remarkable nine-link stretch is covered up to LEU 296, making a jump of more than 60 Å. However, cases of ultra-long-range energy transfer like this are more rare and, at the same time, less efficient. In fact, as a consequence of the rather small amount of energy transferred (nearly 14 kcal mol$^{-1}$), the DB that self-excites at the target site is poorly localized (as in figure 1).

A more efficient transfer event, covering two links (about 11 Å), is analyzed in figure 5. At first, a DB is excited at the kicked site. However, due to interactions with the background, its energy slowly but steadily flows into the system. After approximately 1 ns, about 65% of the excitation energy is still there. At $t = 1.1$ ns, this amount of energy is rapidly and almost entirely transferred to LEU 296, marking the self-localization of another DB. Although the transfer itself is a quite complex process, involving several intermediate sites, it may well prove to be an example of targeted energy transfer [21]. Indeed, as the energy of the DB at the initial site drops, its frequency diminishes as well. This may allow for a transfer to occur if a resonance condition with the frequency of another DB is met. The transmission should be irreversible, as a consequence of both DBs' frequency drifts during energy exchange [21]. Note that, as the energy of the first DB is eroded, the mode becomes also less and less localized [39]. This, in turn, is likely to increase the overlap between the two DB displacement patterns, thus allowing for more efficient energy channeling [4, 8].

To gain further understanding on the transfer mechanism, we investigated energy circulation in a dimeric form of rhodopsin. Very few high-yield and long-range energy transfers were recorded between sites belonging to different monomers, the vast majority of transfer events being confined within the same domain. Indeed, in less than 1% of the...
instances more than 30% of the kick energy (55 kcal mol$^{-1}$) injected at one monomer is transmitted to the other. Here, at variance with most protein dimers, the stiffest regions are located in monomer bulks, so that the edge NMs are localized far away from the interface. This strongly suggests that energy transfers not only target stiff regions, but can also couple any two sites efficiently only through rather stiff channeling pathways. On the other hand, when kicking one of the two (almost) equivalent sites of rhodopsin that are covalently linked to the retinal chromophore, up to about 50% of the excitation energy ends up in a DB localized at one of three specific sites, the targeted location depending upon where (which monomer) the kick is imparted and on the magnitude of the latter. Interestingly, figure 6 reveals that transfer efficiency is optimum in the narrow range 50–55 kcal mole$^{-1}$, i.e. exactly the energy of photons that can be absorbed by the retinal chromophore when it is embedded within rhodopsin ($\lambda = 500 \pm 550$ nm). Moreover, the preferentially targeted residue in this energy range (GLU 113) is known to be involved in the early stages of the signaling cascade following rhodopsin activation [63].

4. Discussion

In summary, despite its coarse-grained nature, the NNM framework is able to provide biologically sensible clues about energy circulation in proteins. High-yield and long-range energy transfers systematically pin energy at the sites the most involved in a small subset of band-edge linear modes, that is, within the stiffest parts of protein structures. These, in turn, are regions preferentially hosting residues involved in catalytic mechanisms [33, 39, 60–62].

In our previous works, the fact that DBs tend to form within the most rigid parts of protein structures had already been underlined. First, by showing that this is where they spontaneously pop up in the course of simulations during which a protein is cooled down as a consequence of friction on its surface residues [33]. Second, by showing that this is where DB analytical solutions can be continued down to arbitrary small energies [39]. Importantly, the latter study also allowed us to show that DBs are able to jump from site to site following energy variations. The present results reveal how efficient this property can be for transmitting energy across protein structures, so that a few key residues are fired at following localized excitations. As a clear example, figure 3 shows that a significant fraction of the energy of a 100 kcal mol$^{-1}$ kick in subtilisin ends up on a single target residue, the stiffest one, for almost every kicked site. Recalling again that active sites have a marked tendency to sit within the stiffest regions [61, 62], what our results suggest is that protein structures may have been designed, during the course of evolution, so as to allow energy to flow where it is needed, e.g. to, or close to catalytic sites. Such extra amounts of energy, with respect to what is commonly available at room temperature, may help crossing rate-limiting energy barriers, thus speeding up catalytic processes by a significant factor. Incidentally, this conclusion is in line with the phylogenetic analysis of structural evolution within protein families, clearly spotlighting the existence of clusters of co-evolving amino acids [64, 65], which may prove associated with preferential energy exchange pathways. Note that such energy transfer processes do not have to be directly linked to conformational changes occurring on the ms time scale, in line with recent results that challenge the very coupling between conformational and chemical transitions in enzymes [66].

However, intensive work remain to be done in order to confirm the above appealing hypothesis. For instance, in order to bridge the gap between the nanosecond time scale of the nonlinear phenomena studied herein and micro to millisecond time scales, which are typical of biologically relevant events occurring within enzymes, DB lifetimes have to be accurately examined, noteworthy as a function of their energy. To this concern, it is interesting to recall that, as a general effect, friction exerted by solvent at the protein surface results in an overall stiffening of the protein bulk [33]. Hence, it is likely, even if somewhat paradoxical, that the lifetimes of DBs harbored in stiff regions could be increased by solvent’s action. Work along this line is in progress.

Of course, demonstrating that DBs are among the key players of enzyme catalysis would also require to consider much more detailed protein models. Indeed, in the framework of NNMs, DBs arise as high-frequency motions of the coarse-grained network. Consequently, since in proteins high-frequency vibrations are localized on chemical bonds and hence behave quantum-mechanically, a semi-classical or even full quantum-mechanical description may prove necessary. Moreover, while we have already shown that DBs are able to arise in the presence of friction acting on nearly half of
the amino acids (those lying on its surface) [33], it is now important to assess how DB properties are influenced by the Brownian noise component of surface forces due to solvent.

As an end remark, we note that, in view of the coarse-grained nature of the NNM scheme, the same site-specific, high-yield and long-range energy transfers observed herein in the case of proteins are also likely to occur in other physical systems, possibly simpler to engineer and to handle, so long as they share with proteins both spatial and stiffness heterogeneity.

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