Parallel P-PD controller to achieve vibration and position control of a flexible beam

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ABSTRACT

Robotic arms are considered as a cantilever beam fixed at one end and due to the length-to-weight ratio, it has a significant vibration-induced that needs to be controlled to achieve accurate position, speed control and to increase its efficiency. In this project, a discretized Timoshenko beam model is used to discuss the dynamics of the system. Further, to implement the control on the hardware an experimental setup is fabricated to observe the open-loop and closed-loop responses of the beam made of low-density polyethylene. An accelerometer as a feedback sensor is attached at one end of the flexible beam while another end is fixed at the moving cart having DC motor as an actuator. Simulink is used as the programming tool to perform all of the experimentation. Proportional-integral-derivative (PID) tuning is performed. Following that open-loop responses of the deflection of the beam parallel to the motion are observed with different input waveforms. By applying a proportional control scheme, another experiment is performed to demonstrate the disturbance rejection with an accelerometer as a feedback sensor, while ignoring position control. Finally, a PD and P based parallel control scheme is proposed to obtain simultaneously both position control and vibration reduction.

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1. INTRODUCTION

This project consists of making a Cartesian robot composed of a flexible beam being moved on guiding rails actuated by a DC motor in order to control the vibration, which is considered one of the major problems of engineering systems [1]. It is necessary to control this vibration in order to reduce energy loss and make the system efficient [2]. The work is divided into different parts such as design, assembly, and development of the control law, for which Ziegler Nichols tuning method of proportional-integral-derivative (PID) is used [3]. The control law must be able to reduce the vibrations of the beam during the motion. The manipulation would possibly consist of a motor, an angular-linear transformation belt, a carriage, and a flexible beam. The deformation of the beam would be captured by an accelerometer while the position is measured with an encoder. Some application of this system includes an automated storage and retrieval systems, robotic links, satellites, airplane wings, and many other systems where cantilever beam is being used.

An observer-based control strategy was proposed by Dadfarnia et al. [4] for a flexible cantilever beam of length 300 mm, having translating base support. PD control is applied for translation control while Lyapunov based controller was designed for controlling the piezoelectric actuator. Hu et al. [5] proposed a
linear quadratic state-feedback regulator and mode theory to minimize vibration of flexible link with piezoelectric actuator and strain gauge transducer. The experimented result emphasized good disturbance rejection and rapid strain reduction. Qiu et al. [6] proposed an accelerometer-based active vibration control for a cantilever beam. A piezoelectric actuator is used for experimental analysis. Non-collocated sensor and piezoelectric actuator dynamical model was derived for designing proportional feedback control of acceleration. Experimental results demonstrated the effectiveness of the proposed control scheme [6]. Song and Gu [7] presented the active vibration control performance of a flexible beam by using piezoceramic sensors and actuators. They adopted a sliding mode controller which has inherent robustness to system parameter variation and external disturbances.

While modelling this kind of complex system, there is always some engineering approximation that comes into consideration. At some points, we ignore dynamics and high-frequency modes (as they have a limited role in determining essential model characteristics than low-frequency modes) to get a reduced system that might result in reduced stability and uncertainties. All such approximation techniques have some pros and cons that enabled us to work with a complex system in constrained space.

In this project, a PD and P based parallel control scheme is proposed to obtain simultaneously both the position control and the vibration reduction. The composition of this report is as follows: Section 2 describes project methodology 3-D modelling, Beam analysis, sensor, actuator, and controller. Section 3 demonstrates a brief description of the experimental setup, and development of the control law. Section 4 discusses the results. Finally, the conclusion is derived from experimentation with discussion on prospects.

2. METHODOLOGY

This section includes the proposed methodology used to control and actuate the system. The dynamic analysis of a flexible beam is briefly discussed along with the finite element analysis. The block diagram representation is discussed to illustrate the working environment for the programming and control.

2.1. Beam model analysis

For the dynamic vibration analysis of the beam, Timoshenko beam model representation is used with discretization parameters [8].

\[
p(z) \frac{\partial^2 w}{\partial t^2} (z,t) = \frac{\partial}{\partial z} \left[ K(z) \left( \frac{\partial w}{\partial z} (z,t) - \phi(z,t) \right) \right], z \in (a, b), t \geq 0 
\]

(1)

\[
l_p(z) \frac{\partial^2 \phi}{\partial t^2} (z,t) = \frac{\partial}{\partial z} \left( E l(z) \frac{\partial \phi}{\partial z} (z,t) \right) + K(z) \left( \frac{\partial w}{\partial z} (z,t) - \phi(z,t) \right) 
\]

(2)

2.1.1. Beam parameters

A low-density polyethylene material beam of 300 mm length, a width of 35 mm, and thickness of 2.5 mm is used in this experiment with material properties of density: 0.92 g/cm³, Young’s modulus: 0.1e-3 GPa, and bulk’s modulus: 1.7 GPa. This beam is fixed on one end with the cart that reduces it is workable length by 40 mm. Beam specifications are shown in Table 1.

| Table 1. Beam specifications |
|-----------------------------|
| Material | low-density Polyethylene |
| Dimensions | 300x35x2.5 mm |
| Density | 0.92 g/cm³ |
| Young’s modulus | 0.1e-3 GPa |
| Bulk’s modulus | 1.7 GPa |

2.1.2. ANSYS simulation for critical analysis

We simulated different types of beams to observe if they met our project specifications. Due to translation, a low force is going to be applied to the beam. Given sensor limitations, we need reasonable deflections/vibration that can be detected and transmitted for analysis. Firstly, we used an aluminium beam of length 300 mm, width 20 mm, and thickness of 1.2 mm. Fixing one side with support and on the other side, applying 0.075 N force in negative Y-direction produced 2.12 mm deformation as shown in Figure 1.

Then reconsidering options, we opted for a low-density polyethylene material-based plastic beam of length 300 mm, the width of 35 mm, and thickness of 3.5 mm. Applying the same force resulted in better deformations around 25 mm. We selected this beam for further analysis as our anticipation for the actual model was to get 20-30 mm deflection in response to applied force as shown in Figure 2.
2.2. 3D Model

To make a base structure for the cart, a 3D model was created as shown in Figure 3. An experimental prototype was fabricated through laser cutting technology on plexiglass material. To move the cart back and forth two translatory guides are passed through the cart. To minimize friction between the cart and the guides 4 linear bearings are added at each side.

2.3. Schematic and block diagram

The motion is provided by a DC motor connected through a belt-pulley drive. The belt is fixed at both ends of the cart to provide direct motion and runs through a free pulley at the other end. The beam is attached to the cart using a nut and bolt. The system schematic is shown in Figure 4 proposes the subsystems:

2.3.1. Sensors

Two sensors are used in this setup. To achieve position feedback, control a hall sensor-based encoder is attached to the motor and used to measure the position in terms of pulse-interrupts through the sensor that measures 29 pulses/cm. To measure the deflection/vibration of the beam an accelerometer is attached at the tip of the beam, where maximum deformation is observed as shown with the finite element analysis tool in the previous section. The accelerometer is configured for 8-bit resolution with 64 counts/g and a maximum range of 2g ($g \approx 9.81 \text{ m/s}^2$) to maintain the trade-off between the resolution, sampling rate, and noise of measurement [9]. The z-axis of the accelerometer is positioned to be along with the motion of the cart. The x-axis is towards the fixed end of the beam and the y-axis towards the base. The deflection sensor can overcome the error of non-collocated sensor modelling that is the limitation of using an accelerometer [10-15].
2.3.2. Actuator

DC motor with an encoder is used as an actuator to provide the motion to the system (cart + beam). The motor specifications are given in the Table 2.

| Parameter       | Value                |
|-----------------|----------------------|
| Related torque  | 0.3 kgf.cm           |
| No-load current | 200 mA max.          |
| No-load speed   | 789 rpm              |
| Stall current   | 2.4 A                |
| Stall torque    | 2.2 kgf.cm           |
| Reduction ratio | 1/19.225             |

2.3.3. Controller

Arduino Mega 2560 is used as the microcontroller to control the system. The communication protocol between Accelerometer and controller is I²C based, while the encoder is communicating through the UART protocol. To program the board, Simulink is used as the programming tool to create a communication channel between the controllers. An external mode-based environment execution allows the users to deploy the block diagram generated codes onto the controller. This feature is useful to observe as well as control the parameters in real-time.

3. EXPERIMENTAL ANALYSIS

In this section, the control methodology is illustrated through Simulink block diagrams. Several control algorithms were adopted to show the different trends of deflection at tip, reference tracking, and control input.

3.1. Position control

The Simulink block diagram shown in Figure 5 is used for reference tracking using PD Controller tuned using the Ziegler Nichols tuning method. The subsystem block of the motor consisting of speed, direction, and switch blocks, is used to drive the motor, that is connected to the controller and power supply by a motor driver. A comparator block is used to determine the direction of the motor from the control signal for the positive or negative control input. A saturation block is used to marginalize the pulse width modulation (PWM) input to the motor speed pin with a range of dead zone (10) and a maximum of 255. These boundary conditions refer to the minimum voltage required by the motor to overcome the static friction and the maximum PWM bandwidth allowed on the controller pin. Encoder block reads the pulses using a hall effect sensor that sends an interrupt signal at every pulse. This output (in pulses) is used to compute the error between the desired and measured positions. By using a multiplying factor, one can directly use the position as input instead of pulses.
3.1.1 Different input signals with x, y, and z deflection data

To observe the beam deflection trends in the x, y, and z-axis, different input signals (sine, square, and triangle) were used in the position feedback control loop as shown in Figure 6. The scope is used to observe the reference tracking. Beam deflection in terms of acceleration in x, y, and z is plotted in a single scope. To make a fair comparison that indicates a maximum change in each axis, the gravitational effect was removed by adding a dead zone block to the output along the y-axis (downwards). Results are shown in section 4 with a brief description.

3.2. Vibration control

To control the vibration/deflection of the beam along the axis of motion, the Simulink control block diagram was developed as shown in Figure 7. The measured beam deflection in terms of acceleration is used to compute the error signal in a P controller-based feedback loop.
3.3. Parallel control

To achieve position and vibration control a parallel feedback loop is proposed to integrate both in a single configuration as shown in Figure 8. Different control inputs can be configured to the system to achieve reference tracking and disturbance rejection. The PD-gain computed from the position feedback is added to the P-gain computed from the vibration feedback. This methodology proved its effectiveness as shown by results in the section.

3.3.1 Disturbance rejection

Disturbance rejection was observed on the parallel control with set position tracking in two ways, one applying the impulse force through Simulink to the system for 0.5 s of an amplitude of 200 as shown in Figure 9. This applies the disturbance to the cart which translates the vibration in the beam passing through the fixed end. In the second method, a force is applied directly to the beam externally causing it to vibrate along the z-axis, the actuator compensates for this disturbance and maintains the position of the cart in both cases.
4. RESULTS

The output data observed from the experiments were plotted through MATLAB figures which represent the trends for deflection of the beam and reference tracking for different cases.

4.1. Position PD control with open loop deflection of beam response and different input waves

Figure 10 shows the responses for the position control feedback. Figure 10 (a) illustrates the reference tracking achieved by the cart with different set-points. Figure 10 (b) shows a step response of the system where data points are marked, to compute the steady-state error (1%), overshoot (1.2%), and settling time (0.3 s). The steady-state error could be minimized by increasing the gain values, but it induces more vibration in the system and is a trade-off between the controller efficiency. Figure 10 (c) shows the control input for reference tracking generated by the PD gain.

![Simulink block diagram for parallel control with disturbance](image)

Figure 9. Simulink block diagram for parallel control with disturbance

![Position feedback control](images)

Figure 10. Position feedback control: (a) reference track, (b) step response, (c) control input for reference tracking

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Figure 11 shows the deflection response with the position control loop. Figure 11 (a) and 11 (b) shows the acceleration of beam in x, y, and z with and without the effect of gravity in the y-axis. Figure 11 (c) shows the zoomed view of the acceleration of the beam along all three axes. It can be seen that the least vibration is observed in the axis towards the base as there is no motion along that axis. A limited vibration is observed along the axis towards the fixed end of the beam mostly in the positive direction (towards the fixed end). However, a significant vibration is observed along the axis of motion that oscillates in the positive and negative direction with the maximum oscillations. Therefore, with the mentioned observations, acceleration along the z-axis was chosen to control the vibration of the beam and to calculate controller gain for the actuator input.

Figure 11: Open-loop beam deflection (x, y, z) response in terms of acceleration: (a) with the gravity effect and (b) without the gravity effect in terms of acceleration, and (c) the zoomed view

4.1.1. Sine wave

Figure 12 shows the system response when a sine wave is selected as the input signal for reference tracking. Figure 12 (a) shows the reference tracking for the sine wave of varying frequency and amplitude. Figure 12 (b) demonstrates the measured acceleration of the beam tip along the axis of motion, it can be seen that it is lesser with a lower frequency and increases with increasing frequency and amplitude. Figure 12 (c) shows the control input generated by the controller for the position control to track the sine wave, it can be concluded that the control input required is more for lesser frequency than the higher frequency for the same amplitude.
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4.2. Vibration P and PD control

After observing the open-loop deflection responses from various input signals, the Ziegler Nichols tuning method was adopted to iterate for the best gain values. First P-gain was selected to check the response and then later the PD-gain. The difference in vibration/deflection trend is shown in Figure 15 (a) for open-loop with 4 s of settling time, P closed-loop with 2 s of settling time, and PD closed-loop with 1.6 s of settling time. Figure 15 (b) shows the control input for P and PD controllers. It can be seen that the control input required for the PD controller is more than the P controller. Therefore, to consider the settling time and control input P controller was adopted to design an efficient controller.

4.3. Parallel Control

Figure 16 shows the responses for position and vibration control loop using P and PD gains respectively, integrated using a parallel control loop. Figure 16 (a) demonstrates the reference tracking. Figure 16(b) illustrates the step response of the system with a steady-state error of 0.14%, overshoot of 6.4%, and the settling time of 1.7 s. The overshoot is greater than the response with no acceleration feedback, however, the other parameters are lesser. The overshoot signifies the increased instability required to stabilize the system at the end of the motion. Figure 16 (c) shows the deflection at the tip of beam responses without and with feedback. Figure 16 (d) demonstrates the control input needed to stabilize the system; it can be seen that the control input for parallel loop requires constant input to minimize the vibration during the motion.
Figure 16. System response with parallel control for position and acceleration feedback: (a) reference tracking with and (b) step response for beam position and deflection control, (c) deflection (z) response, and (d) control input

4.3.1 Disturbance rejection
The results were obtained for the disturbance rejection applied by two methods. Figure 17 (a) shows set-point control after an impulse of amplitude 200 is applied to the system (directly to the cart which transfers the vibration to the beam) for 0.5 s. The settling time to reach back to the set position was observed to be 1.7 s with a steady-state error of 0.11%. Figure 17 (b) demonstrates the vibration control for the same impulse force with a settling time of 2.1 s for the vibration to be completely zero. Figure 17 (c) illustrates the disturbance rejection for position control when the external disturbance is applied directly to the beam inducing vibration. It can be observed that the settling time is 1.2 s. Figure 17 (d) shows the disturbance rejection for vibration with the same external force which makes the settling time to be 1.8 s.

Figure 17. Parallel control with disturbance rejection: (a) position control and (b) beam deflection control for impulse disturbance, and (c) position control and (d) beam deflection control for external disturbance

5. CONCLUSION AND FUTURE WORK
A parallel P-PD controller scheme is discussed in this report to achieve the vibration and position control of a flexible beam. The open-loop trends of beam deflection along the axis of motion (z) are shown with the position feedback loop applying different input wave signals (sine, square, and triangle). Later, to
control the vibration of the beam, an acceleration feedback loop is designed to stabilize the beam vibration/deflection of the beam. After observing the trend and tuning through the Ziegler Nichols method a parallel feedback control block diagram is modelled to achieve position reference tracking along with the vibration control. The real-time hardware implementation is achieved, and the responses were shown through plotted graphs of reference tracking, deflection (z), and control input to the actuator. In the future, other control strategies can be applied to minimize the error and achieve better stabilization and robustness. To minimize the noise and error in measurement, a deflection sensor (piezo or strain gauge) can be used at the fixed end of the beam by using sensor fusion.

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