We experimentally and theoretically study phase coherence in two-component Bose-Einstein condensates of $^{87}$Rb atoms on an atom chip. Using Ramsey interferometry we measure the temporal decay of coherence between $|F = 1, m_F = -1\rangle$ and $|F = 2, m_F = +1\rangle$ hyperfine ground states. We observe that the coherence is limited by random collisional phase shifts due to the stochastic nature of atom loss. The mechanism is confirmed quantitatively by a quantum trajectory method based on a master equation which takes into account collisional interactions, atom number fluctuations, and losses in the system. This decoherence process can be slowed down by reducing the density of the condensate. Our findings are relevant for experiments on quantum metrology and many-particle entanglement with Bose-Einstein condensates and the development of chip-based atomic clocks.

Atomic Bose-Einstein condensates (BECs) in magnetic traps are exceptionally well-isolated quantum many-body systems. Distinct from most other systems, the coherence of atomic BECs in state-of-the-art experiments is limited by intrinsic dynamics rather than interactions with the environment [1]. Elucidating the dominant decoherence mechanisms is thus an intriguing challenge for quantum many-body physics, but at the same time also highly relevant for applications of BECs in quantum metrology [2] and in experiments on the foundations of quantum physics [3–6].

The spatial coherence across a condensate has been studied in different systems [7–10]. Here we focus on the temporal coherence of three-dimensional trapped BECs, which limits the preparation fidelity of non-classical states and the duration of interferometric sequences in precision measurements. Theoretical studies of BEC temporal coherence have suggested different decoherence mechanisms resulting from the interplay of elastic collisional interactions, inelastic collisional atom loss, and finite temperature [11]. Previous experiments have mostly investigated inhomogeneous dephasing due to mean-field driven spatial dynamics of the condensate wavefunctions [11] [12], while homogenous dephasing was attributed to technical noise. Inhomogeneous dephasing and spatial demixing can be reversed by spin echo techniques [11] [11]. Other experiments investigated the effect of phase noise on spin-squeezed states [11]. However, a detailed experimental study of the predicted homogeneous phase decoherence mechanisms [1], which fundamentally limit the BEC coherence, has not yet been reported.

Here we report experiments and corresponding theoretical simulations of the decoherence mechanisms in two-component BECs of $^{87}$Rb atoms. Using Ramsey interferometry, we explore the phase coherence of the hyperfine ground states $|1\rangle \equiv |F = 1, m_F = -1\rangle$ and $|2\rangle \equiv |F = 2, m_F = +1\rangle$ in a magnetic trap on an atom chip [14]. This system is used in recent experiments on quantum metrology and many-particle entanglement [3–4] [15] as well as in chip-based atomic clocks that are currently being developed [13] [16]. We observe an increase of relative phase fluctuations between the two hyperfine states (Fig. 1), and find that the coherence is limited by random collisional phase shifts due to the stochastic nature of atom loss. The experimental results are confirmed quantitatively by a theoretical model based on the quantum trajectory approach, which takes into account elastic collisional interactions, atom number fluctuations, and losses in the system. Our experimental findings are relevant for compact atomic clocks realized in similar cold or ultracold atomic systems where atomic interactions are a limiting factor [13] [16].

In our experiment, a BEC of $10^{20} \pm 40$ $^{87}$Rb atoms is prepared in the hyperfine state $|1\rangle$ and trapped in a cigar-shaped magnetic potential with harmonic trapping frequencies $\omega_{r,z} = 2 \pi \times (714, 114)$ Hz. We coherently couple the two hyperfine states $|1\rangle$ and $|2\rangle$ via a resonant two-photon transition induced by microwave and radio-frequency magnetic fields, with a two-photon Rabi frequency of $\approx 2 \pi \times 600$ Hz at a detuning of $\approx 2 \pi \times 500$ kHz from the intermediate state $|F = 2, m_F = 0\rangle$. The two states $|1\rangle$ and $|2\rangle$ are of special interest for atomic clocks because their differential Zeeman shift vanishes to first order at a magnetic field of $\approx 3.23$ G, making superpositions of the two states largely insensitive to magnetic field fluctuations [17]. Since the atoms are condensed in a single spatial mode, they can be regarded as pseudo-spin $1/2$ and the whole ensemble can be well described in terms of a collective spin [2].

In order to investigate the phase coherence between the two spin states, we perform a Ramsey interferometer sequence with varying interrogation time. Starting with a BEC in state $|1\rangle$, we apply a $\pi/2$-pulse to prepare...
Ramsey fringe

\[ n_{\text{rel}}(\phi_R) = V \sin(\phi_R + \phi), \quad (1) \]

where \( V \) is the fringe visibility, and \( \phi \) is a classical random variable describing the phase accumulated by the state during the interrogation time \( T_R \), which fluctuates due to noise. The phase noise quantified by the standard deviation \( \Delta \phi \) is evaluated in the following way.

For short Ramsey times \( T_R < 0.2 \text{ s} \), we experimentally set the Ramsey phase to the value \( \phi_R = \phi_0 \) where the mean of \( n_{\text{rel}} \) is zero. At this point, with the maximal slope of the fringe \( \partial n_{\text{rel}} / \partial \phi = V \), the phase is evaluated as \( \phi = \arcsin(n_{\text{rel}} / V) \). In general, \( V < 1 \) due to the asymmetric losses in the two spin states. We repeat the experiment to gather statistics and evaluate the standard deviation \( \Delta \phi \) assuming a Gaussian distribution of the phase fluctuations.

For long Ramsey times \( T_R > 0.2 \text{ s} \), the above method is not reliable due to ambiguities of the phase. As a more reliable evaluation, we fit the entire Ramsey fringe with \( n_{\text{rel}}(\phi_R) = C \sin(\phi_R - \phi_0) \), where \( C \) is the contrast, and \( \phi_0 \) is the fitted phase at zero-crossing. For a Gaussian distribution of the phase fluctuations, \( \Delta \phi \) is evaluated by the relation \( C = V \exp(-\frac{1}{2} \Delta \phi^2) \).

We observe an increase of the phase noise with time (Fig. 1). The main interest of this work is to investigate the origins of these fluctuations, which can be divided into technical and intrinsic sources of noise. On the technical side, the system is suffering from local oscillator noise, magnetic field fluctuations, and detection noise. To estimate the contribution of technical noise, we perform the same experiments with non-condensed atoms in a relaxed trap with frequencies \( (\omega_r, \omega_z) = 2\pi \times (301, 113) \text{ Hz} \). The non-condensed atoms suffer from the same technical noise, but due to a significantly reduced atomic density, the effects of interactions are largely suppressed. We use the result as an upper bound on the technical noise in our experiment, shown in Fig. 1 with a black dashed line \( \Delta \phi_{\text{tech}}(t) = 0.1 \text{ (rad/s) } t \). This demonstrates that technical noise contributes little to the observed phase noise in our experiments.

Intrinsic to the two-component BEC, the collisional interactions also introduce phase fluctuations. The dynamics of the collective spin due to elastic collisions between atoms can be described by the Hamiltonian \([18]\):

\[ \hat{H} = \hbar \chi \hat{N} \hat{S}_z + \hbar \chi \hat{S}_z^2, \quad (2) \]

where \( \hat{S}_z = (\hat{N}_1 - \hat{N}_2)/2 \) is the z component of the collective spin operator, and \( \hat{N} = \hat{N}_1 + \hat{N}_2 \) is the total atom number. The parameters \( \chi = \frac{1}{2N} \left( \frac{\partial^2 E}{\partial N_1^2} - \frac{\partial^2 E}{\partial N_2^2} \right) \) and \( \chi = \frac{1}{2N} \left( \frac{\partial^2 E}{\partial N_1 \partial N_2} - 2 \frac{\partial^2 E}{\partial N_1^2} \right) \) depend on the energy \( E \) of the two interacting components with mean atom number \( \bar{N}_1 \) and \( \bar{N}_2 \) in state \( |1\rangle \) and \( |2\rangle \) respectively \([15]\).
In our experiment where the atoms occupy a single spatial mode, the first term $\hbar \chi N \hat{S}_z$ dominates (typical values: $\chi/2\pi \approx 4.8 \times 10^{-4}$ Hz and $\chi/2\pi \approx 0.01$ Hz). This term introduces a phase evolution depending on the total atom number $N$, which is the so-called collisional clock shift [12, 19]. Since the initial atom number of the BEC fluctuates, a superposition state has a spread of phase evolution rates, causing dephasing. As a result, for a fixed $T_R$, the measured phase $\phi$ shows a linear dependence on the total atom number $N$ (see Fig. 2(a)), which can be extracted by fitting the data with the function

$$f(N) = \alpha(T_R)T_R N + \beta,$$

where $\alpha(T_R)$ and $\beta$ are free parameters. The value we obtain for $\alpha(T_R)$ can be used to quantify the strength of the collisional phase shifts. In the ideal case with $\chi = 0$ and without atom loss, $\alpha(T_R)T_R N$ is proportional to $\int_0^{T_R} \chi(t)N(t)dt$.

As is common in atomic clock experiments, one can enhance the precision of the phase measurement by post-processing the data to subtract the dependence of the phase on $N$. The corrected phase $\phi_{\text{corr}} = \phi - \alpha(T_R)T_R N$, as plotted in Fig. 2(c), shows no dependence on $N$. This correction reduces the observed phase noise significantly, as shown in Fig. 1(c, d) and Fig. 2(c, d). However, even after the clock-shift correction, there is still significant residual phase noise, which can be attributed to the random nature of atom loss. Atom loss due to inelastic collisions occurs stochastically, thus randomizing the atom number time-evolution. In general, this leads to phase fluctuations since experimental shots with different atom number time-evolution will dephase with respect to each other. Experimentally, only the final total atom number is accessible, therefore the correction method described above does not allow to subtract the random collisional phase shifts completely.

To build a theoretical model taking into account this interplay of collisional interactions and the stochastic nature of atom losses, we model the quantum dynamics of the collective spin with the master equation [20]:

$$\frac{d\hat{\rho}}{dt} = -\frac{i}{\hbar} [\hat{H},\hat{\rho}] + \sum_{k=1}^{4} \hat{C}_k \hat{\rho} \hat{C}_k^\dagger - \frac{1}{2} \hat{\rho} \hat{C}_k^\dagger \hat{C}_k - \frac{1}{2} \hat{C}_k \hat{C}_k^\dagger \hat{\rho},$$

where the Hamiltonian is defined in Eq. (2).

The dominant types of losses are collisions between the BEC atoms and the residual background gas, described by one-body loss constant $K_1$, and the intrinsic losses from inelastic two-body collisions, described by inter-species and intra-species two-body loss constants $K_{12}^{(2)}$ and $K_{12}^{(2)}$, respectively. Two-body loss in state $|1\rangle$ and three-body losses are negligible for our parameters. The quantum jump operators $\hat{C}_k$ express the four types of significant losses in our system: one-body losses ($\hat{C}_1$, $\hat{C}_2$) = ($\sqrt{K_1}a_1$, $\sqrt{K_1}a_2$) and two-body losses ($\hat{C}_3$, $\hat{C}_4$) = ($\sqrt{K_2}a_1a_2$, $\sqrt{K_2}a_2^2$), where $a_i$ is the bosonic operator annihilating atoms in the $|i\rangle$ state. Parameters $\gamma_{ij}$ are the integrated two-body loss rates, i.e. $\gamma_{ij} = K_{ij}^{(2)} \int d^3r |\psi_i|^2 |\psi_j|^2$, where $|\psi_i|^2$ is the wavefunction of state $|j\rangle$.

In order to quantify the atom loss in our experiment, we perform three independent measurements. First, we prepare a BEC in state $|1\rangle$. With the loss of atoms happening solely due to one-body losses, we can extract $K_1$ by a simple exponential fit, shown in Fig. 3 top panel. In a second experiment, we measure the loss of atoms starting with a BEC in $|2\rangle$. In this case, there are one-body losses with already determined rate $K_1$ and the interspecies two-body losses depending on $K_{12}^{(2)}$. We solve the one-component Gross-Pitaevskii equation (GPE) including losses with varying $K_{12}^{(2)}$ to find the best fit to the experimental data, see Fig. 3 middle. Eventually, we perform experiments with the BEC prepared in an equal superposition of $|1\rangle$ and $|2\rangle$ (Fig. 3 bottom). In this case all loss channels are present, but only one unknown loss constant $K_{12}^{(2)}$ remains, which we determine by comparing the two-component GPE (2C-GPE) simu-

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**FIG. 2.** Interferometer data (a,c) and histogram (b,d) at fixed time $T_R = 100$ ms and fixed $\phi_R$, with the raw data (red) and data after the correction of collisional phase shift (blue). Black curves are a linear fit of the data. The raw $\phi$ shows a dependence on $N$, while after correction the slope is zero. (d) shows a reduced phase uncertainty compared to (b) due to the correction. (e) shows the collisional phase shift coefficient $\alpha$ at different times in a tight trap $\omega_{r,z} = 2\pi \times (714, 114)$ Hz (red) and a shallow trap $\omega_{r,z} = 2\pi \times (301, 113)$ Hz (purple). The dashed curves with corresponding colors show the results of the quantum trajectory simulation.
FIG. 3. Time evolution of the mean atom number for three different initial states: all atoms in state |1⟩ (top), all atoms in state |2⟩ (middle) and atoms initially in the superposition \((|1⟩ + |2⟩)/\sqrt{2}\) (bottom). Red (Blue) points show the measured atom number in state |1⟩ (|2⟩). Lines are from corresponding GPE simulations with loss rate constants \(K_1 = 0.17 \text{ s}^{-1}\), \(K_2^{(2)} = 10.3 \times 10^{-14} \text{ cm}^3\text{s}^{-1}\) and \(K_{12}^{(2)} = 2.0 \times 10^{-14} \text{ cm}^3\text{s}^{-1}\).

an approach assumes that the atomic densities follow adiabatically the 2C-GPE ground states and the superposition states with different atom loss trajectories evolve with the same parameters \(\chi(t), \tilde{\chi}(t), \text{and } \gamma_{ij}(t)\).

The phase noise simulation starts with an equal superposition of the two spin states. The initial number of atoms is drawn from a Gaussian distribution with mean and standard deviation as in the experiment. Its dynamics, given by Eq. (4), is found with the help of the quantum trajectory method \cite{25, 26}. This stochastic method results in a set of random final states \(\{\hat{\psi}(T_R)\}\), whose mixture is the solution of the master equation, i.e. \(\sum |\hat{\psi}(T_R)\rangle\langle\hat{\psi}(T_R)| = \hat{\rho}(T_R)\). The numerically found stochastic wave-functions are treated as experimental realizations – we analyze them in exactly the same manner as the real measurements to extract contrast, visibility, clock-shift correction and phase noise, to ensure a reliable comparison between experiment and simulation.

In Fig. 4 we show the results of the quantum trajectory simulations. The simulation accurately reproduces the observed increase of phase noise, both before and after the phase shift correction. We also show in Fig. 2(c) the simulated and measured collisional phase shift as a function of time. In conclusion, the simulation provides a good description of the mean of phase shift, as well as the phase fluctuations.

Our study shows that the phase coherence is limited mainly by the interplay of collisional interactions (elastic and inelastic) between atoms. To extend the coherence time, one can decrease the gas density, and thereby reduce the collisional rates. We confirm this by performing the phase noise measurement in a relaxed trap with trap frequencies \(\omega_{(r,z)} = 2\pi \times (301, 113) \text{ Hz}\). As shown in Fig. 4(d) the phase noise is indeed strongly reduced. In order to reach the fundamental bound of precision limits in quantum metrology as theoretically described

FIG. 4. Comparison of the extracted initial \(\tilde{\chi}\) between experiment (black dots) and 2C-GPE simulation (red line). For BECs with varying initial atom numbers we extract \(\tilde{\chi}\) with a Ramsey sequence of \(T_R = 10 \text{ ms}\).
in [21, 22], the unwanted effects of decoherence should be further mitigated. Experimentally, a state-dependent potential could be applied to engineer interactions [18]. Using this technique, one can minimize $\chi$, thus the collisional phase shift, or tune the interactions so that the quantum states are protected from the decoherence induced by two-body losses, as proposed in [23].

In conclusion, we measure precisely the growth of the phase noise in a trapped two-component BEC and identify the main decoherence sources. A clear distinction is drawn between the technical noise and the noise induced by the atomic interactions. We observe that the coherence is limited by random collisional phase shifts due to the stochastic nature of atom loss. The good agreement between our data and the GPE simulation also allows us to extract the two-body loss rate constants. Our experimental findings provide a good understanding of the temporal coherence of a two-component BEC. In contrast to most other systems where decoherence is due to interactions with the environment, in our experiment the atoms are well-isolated, and the observed decoherence effect is intrinsic to such a two-component BEC. Our findings are relevant for trapped-atom clocks and interferometers where the atomic interactions play important roles [13].

We acknowledge discussions with C. Salomon, A. Sinatra, and J. Reichel. We are grateful to Baptiste Alazard for discussions and contributions to this work at an early stage. This work was supported by the Swiss National Science foundation. Y. L. acknowledges support of a scholarship from the China Scholarships Council (No. 201806210182). K. P. and P. T. acknowledge networking support by the COST Action CA16221. Center for Theoretical Physics, Polish Academy of Sciences is a member of the National Laboratory of Atomic, Molecular and Optical Physics (KL FAMO).

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