On the theoretical and experimental uncertainties in the extraction of the $J/\psi$ absorption cross section in cold nuclear matter

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Abstract. We investigate the cold nuclear matter effects on $J/\psi$ production, whose understanding is fundamental to study the quark-gluon plasma. Two of these effects are of particular relevance: the shadowing of the parton distributions and the nuclear absorption of the $c\bar{c}$ pair. If $J/\psi$’s are not produced via a $2 \rightarrow 1$ process as suggested by recent theoretical works, one has to modify accordingly the way to compute the nuclear shadowing. This naturally induces differences in the absorption cross-section fit to the data. A careful analysis of these differences however requires taking into account the experimental uncertainties and their correlations, as done in this work for $dAu$ collisions at $\sqrt{s_{NN}} = 200$ GeV, using several shadowing parametrisations.

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1. Introduction

Relativistic nucleus-nucleus ($AB$) collisions are expected to produce a deconfined state of QCD matter – the Quark Gluon Plasma (QGP) – at high enough densities or temperatures. It has long been suggested [1] that the $J/\psi$ meson would be sensitive to Hot and Dense Matter (HDM) effects, through mechanisms like the dissociation of
Uncertainties in the extraction of $\sigma_{J/\psi}^{\text{abs}}$ in cold nuclear matter

the $c\bar{c}$ pair due to the colour Debye screening. A significant suppression of the $J/\psi$ yield was observed by the PHENIX experiment in CuCu [2] and AuAu [3] collisions at $\sqrt{s_{NN}} = 200$ GeV. However, before giving any interpretation, Cold Nuclear Matter (CNM) effects have to be properly disentangled and subtracted. They are known to impact the $J/\psi$ production in proton-nucleus ($pA$) or deuteron-nucleus ($dA$) collisions, where the deconfinement conditions can not be reached. Such non-trivial effects are demonstrated by the PHENIX $dA$ data [4] obtained at the same energy. Two CNM effects are of particular importance [5]: (i) the shadowing of the initial parton distributions (PDFs) due to the nuclear environment, and (ii) the breakup of $c\bar{c}$ pairs consecutive to multiple scatterings with the remnants of the projectile and target nuclei, referred to as the nuclear absorption. Recent theoretical works incorporating QCD corrections or $s$-channel cut contributions have emphasized [6, 7] that the Colour-Singlet (CS) mediated contributions are sufficient to describe the experimental data for hadroproduction of both charmonium and bottomonium systems without the need of Colour-Octet (CO) contributions. Furthermore, recent works [8] focusing on production at $e^+e^-$ colliders have posed stringent constraints on the size of CO contributions, which are the precise ones supporting a $2 \rightarrow 1$ hadroproduction mechanism [9]. As a consequence, $J/\psi$ production at low and mid $P_T$ likely proceeds via a $2 \rightarrow 2$ process, such as $g + g \rightarrow J/\psi + g$, instead of a $2 \rightarrow 1$ process. As we have shown in previous studies [10, 11, 12], this modifies both the way to compute the nuclear shadowing and its expected impact on the $J/\psi$ production. In this work, we shall focus on the changes induced on the rapidity dependence of the $J/\psi$ nuclear modification factor in $dA$, while using several parametrisations of the nuclear PDF. As in [4] – where CNM effects were computed based on a $2 \rightarrow 1$ kinematics – we shall use the same $dA$ data to derive the absorption cross-section $\sigma_{\text{abs}}$ required on top of the shadowing, but assuming here a $2 \rightarrow 2$ underlying partonic process. We shall compare the results found in both schemes, with a special emphasis on the limitations from the experimental uncertainties.

The article is organized as follows. In section 2, we will describe our model and the method chosen to carry a data-driven evaluation of the nuclear absorption cross-section. And in section 3, we will present and discuss our results before concluding.

2. Our approach

To describe the $J/\psi$ production in nucleus collisions, our Monte Carlo framework [10, 13] is based on the probabilistic Glauber model, the nuclear density profiles being defined with the Woods-Saxon parameterisation for any nucleus $A > 2$ and the Hulthen wavefunction for the deuteron [14]. The nucleon-nucleon inelastic cross section at $\sqrt{s_{NN}} = 200$ GeV is taken to $\sigma_{NN} = 42$ mb and the maximum nucleon density to $\rho_0 = 0.17$ nucleons/fm$^3$.

In order to study the $J/\psi$ production, we need to implement in our Monte Carlo the following ingredients: the partonic process for the $c\bar{c}$ production and the CNM effects.
2.1. Partonic process for the $c\bar{c}$ production

Most studies on the $J/\psi$ production in hadronic collisions rely on the assumption that the $c\bar{c}$ pair is produced by the fusion of two gluons carrying some intrinsic transverse momentum $k_T$. The partonic process being a $2 \rightarrow 1$ scattering, the sum of the gluon intrinsic transverse momentum is transferred to the $c\bar{c}$ pair, thus to the $J/\psi$ since the soft hadronisation process does not alter significantly the kinematics. This is supported by the picture of the Colour Evaporation Model (CEM) at LO (see [9] and references therein) or of the CO mechanism at $\alpha_s^2$ [15]. In such approaches, the transverse momentum $P_T$ of the $J/\psi$ entirely comes from the intrinsic transverse momentum of the initial gluons.

However, the average value of $k_T$ is not expected to go much beyond $\sim 1$ GeV. So this process is not sufficient to describe the $P_T$ spectrum of quarkonia produced in hadron collisions [9]. For $P_T \gtrsim 2-3$ GeV, most of the transverse momentum should have an extrinsic origin, i.e. the $J/\psi$'s $P_T$ would be balanced by the emission of a recoiling particle in the final state. The $J/\psi$ would then be produced by gluon fusion in a $2 \rightarrow 2$ process with emission of a hard final-state gluon. This emission, which is anyhow mandatory to conserve C-parity, has a definite influence on the kinematics of the $J/\psi$ production. Indeed, for a given $J/\psi$ momentum (thus for fixed rapidity $y$ and $P_T$), the processes discussed above, i.e. $g + g \rightarrow c\bar{c} \rightarrow J/\psi (+X)$ and $g + g \rightarrow J/\psi + g$, will proceed on the average from initial gluons with different Bjorken-$x$. Therefore, they will be affected by different shadowing corrections. From now on, we will refer to the former scenario as the intrinsic scheme, and to the latter as the extrinsic scheme.

In the intrinsic scheme, we use the fits to the $y$ and $P_T$ spectra measured by PHENIX [17] in $pp$ collisions at $\sqrt{s_{NN}} = 200$ GeV as inputs of the Monte-Carlo. Indeed, the measurement of the $J/\psi$ momentum completely fixes the longitudinal momentum fraction carried by the initial partons:

$$x_{1,2} = \frac{m_T}{\sqrt{s_{NN}}} \exp(\pm y) \equiv x_{1,2}^0(y, P_T),$$

with the transverse mass $m_T = \sqrt{M^2 + P_T^2}$, $M$ being the $J/\psi$ mass.

On the other hand, in the extrinsic scheme, information from the data alone – the $y$ and $P_T$ spectra – is not sufficient to determine $x_1$ and $x_2$. Actually, the presence of a final-state gluon introduces further degrees of freedom in the kinematics, allowing several $(x_1, x_2)$ for a given set $(y, P_T)$. The four-momentum conservation explicitely results in a more complex expression of $x_2$ as a function of $(x_1, y, P_T)$:

$$x_2 = \frac{x_1 m_T \sqrt{s_{NN}} e^{-y} - M^2}{\sqrt{s_{NN}} \sqrt{s_{NN} x_1 - m_T e^y}}.$$

Equivalently, a similar expression can be written for $x_1$ as a function of $(x_2, y, P_T)$. Even if the kinematics determines the physical phase space, models are anyhow mandatory to compute the proper weighting of each kinematically allowed $(x_1, x_2)$. This weight is simply the differential cross section at the partonic level times the gluon PDFs, i.e. $g(x_1, \mu_F) g(x_2, \mu_F) d\sigma_{gg \rightarrow J/\psi + g} / dy dP_T dx_1 dx_2$. In the present implementation of our
2.2. Shadowing and nuclear absorption

To obtain the $J/\psi$ yield in $pA$ and $AA$ collisions, a shadowing-correction factor has to be applied to the $J/\psi$ yield obtained from the simple superposition of the equivalent number of $pp$ collisions. This shadowing factor can be expressed in terms of the ratios $R_i^A$ of the nuclear Parton Distribution Functions (nPDF) in a nucleon belonging to a nucleus $A$ to the PDF in the free nucleon:

$$R_i^A(x,Q^2) = \frac{f_i^A(x,Q^2)}{A f_i^{\text{nucleon}}(x,Q^2)} , \quad i = q, \bar{q}, g .$$  \hspace{1cm} (3)

The numerical parameterisation of $R_i^A(x,Q^2)$ is given for all parton flavours. Here, we restrict our study to gluons since, at high energy, the $J/\psi$ is essentially produced through gluon fusion [9]. In order to see how the CNM effects can vary depending on the different shadowing parametrisations used as an input, we will consider three of them: nDSg [18] at LO, EKS98 [19] and EPS08 [20]. They span the current evaluation of the uncertainty [21] on the gluon nPDF, from a small to a very large antishadowing.

The second CNM effect that we are going to take into account concerns the nuclear absorption. In the framework of the probabilistic Glauber model, this effect is usually parametrised by introducing an effective absorption cross section $\sigma_{\text{abs}}$ of the pre-resonant $c\bar{c}$ pair when propagating in the nuclear medium. In the following, we shall compare the data-constrained values of $\sigma_{\text{abs}}$ given two different partonic $c\bar{c}$ production mechanisms – intrinsic and extrinsic – and three shadowing parametrisations as cited above.

2.3. A data-driven evaluation of the nuclear absorption cross-section

We present here the derivation of the $\sigma_{\text{abs}}$ values consistent with the PHENIX $dAu$ data, taking into account the various experimental uncertainties and their correlations. To do so, we have chosen to follow the procedure from [4, 22]. For a given choice of the $c\bar{c}$ production mechanism and nPDF parametrisation, the best possible agreement of the theory to the data is obtained for the value of $\sigma_{\text{abs}}$ that minimizes the quantity:

$$\chi^2(\vec{p}, \epsilon_b, \epsilon_c) = \sum_{i=1}^{n} \left( \frac{d_i + \epsilon_b \sigma_b + \epsilon_c d_i \sigma_c - \mu_i(\vec{p})}{\tilde{\sigma}_i} \right)^2 + \epsilon_b^2 + \epsilon_c^2$$  \hspace{1cm} (4)

with $\tilde{\sigma}_i = \sigma_i (d_i + \epsilon_b \sigma_b + \epsilon_c d_i \sigma_c)$, $d_i$ being the set of experimental values from PHENIX, $\mu_i$ the respective values predicted by the theory for a given set of parameters $\vec{p}$ (i.e. the nPDF parametrisation and $\sigma_{\text{abs}}$), $\sigma_i$ are the point-to-point uncorrelated errors (statistical and systematic), $\sigma_b$ the point-to-point correlated systematic errors, $\sigma_c$ the global systematic error on the normalisation of the data and $\epsilon_{(b,c)}$ the fractions of the systematic uncertainties $\sigma_{(b,c)}$ used to shift the data points $d_i$. 
3. Results and discussion

In the following, we present our results for the $J/\psi$ nuclear modification factor in $dAu$ collisions: $R_{dAu} = dN_{dAu}^{J/\psi}/\langle N_{coll} \rangle dN_{pp}^{J/\psi}$, where $dN_{dAu}^{J/\psi}(dN_{pp}^{J/\psi})$ is the observed $J/\psi$ yield in $dAu$ ($pp$) collisions and $\langle N_{coll} \rangle$ is the average number of nucleon-nucleon collisions occurring in one $dAu$ collision. Without nuclear effects, $R_{dAu}$ should equal unity.

| Scheme         | $\sigma_{abs}$ (mb) | $\chi^2_{min}$ | $\sigma_{abs}$ (mb) | $\chi^2_{min}$ |
|----------------|---------------------|-----------------|---------------------|-----------------|
| nDSg Int.      | $2.2^{+2.8}_{-2.2}$ | 1.6             | nDSg Ext.           | $3.0^{+2.5}_{-2.4}$ | 1.4           |
| EKS98 Int.     | $3.2 \pm 2.4$       | 0.9             | EKS98 Ext.          | $3.9^{+2.7}_{-2.4}$ | 1.1           |
| EPS08 Int.     | $2.1^{+2.6}_{-2.2}$ | 1.1             | EPS08 Ext.          | $3.6^{+2.4}_{-2.5}$ | 0.5           |

Table 1: $\sigma_{abs}$ extracted from fits of $R_{dAu}$ vs $y$ for the intrinsic (left) and extrinsic (right) schemes, when considering all the different types of errors on the data, together with the corresponding $\chi^2$ obtained for the best fit.

In Table 1, we recall the results from [12], with the value of $\sigma_{abs}$ corresponding to the best fit to PHENIX data $R_{dAu}$ vs $y$, and the one standard deviation uncertainties. As in [4], this extraction relies on the assumption that $\sigma_{abs}$ is independent of $y$. The best agreement to the data is obtained in the extrinsic scheme with EPS08. The larger is the antishadowing, the larger are the differences between both schemes. This is visible in the $\chi^2$ for the best fit or on the different shapes of the curves in Fig. 1 which shows the obtained CNM effects together with PHENIX data for $R_{dAu}$ vs $y$. In this plot, the anti-shadowing peak in $R_{dAu}$ is systematically shifted towards larger $y$ for the extrinsic scheme with respect to the one in the intrinsic case. This reflects the larger value of the gluon momentum fraction $x_2$ in the Au nucleus needed to produce a $J/\psi$ when the momentum of the final state gluon is indeed accounted for. We shall now focus on the bands picturing the CNM effects in both schemes which account for the experimental uncertainties. For the time being, the current size of the errors unfortunately does not allow to distinguish between the two approaches if assuming a constant $\sigma_{abs}$ with $y$.

Using the same procedure, we have qualitatively studied three scenarios with thirty times more statistics and a) no improvement, b) a reduction of 35% and c) a reduction of 50% of the systematics. We have found that, with the same assumption on $\sigma_{abs}$ (namely constant vs $y$), the latest $dAu$ data (2008) will not be sufficient to distinguish between a $2 \rightarrow 1$ and a $2 \rightarrow 2$ production mechanism by only looking at the $y$-dependence of $R_{dAu}$, unless the (anti)shadowing is as strong as encoded in the EPS08 parametrisation.

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Uncertainties in the extraction of $\sigma_{J/\psi}^{\text{abs}}$ in cold nuclear matter

Figure 1: $R_{dA}$ vs $y$ for the intrinsic and extrinsic schemes and for the three nPDF parametrisations, compared to PHENIX data [4]. For each scheme, the central band represents the range in $\sigma_{\text{abs}}$ consistent with the data within one standard deviation, when taking into account the point-to-point uncorrelated (bar) and correlated (box) errors. The corresponding $\sigma_{\text{abs}}$ values are reported in the legend. The outer band is the obtained range in $\sigma_{\text{abs}}$ when the global error on the data normalisation is also considered.

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