Electric Field Dependence of Topological Edge States in One-Bilayer Bi(111): A First-Principles Study

Hikaru Sawahata† and Naoya Yamaguchi
Graduate School of Natural Science and Technology, Kanazawa University, Kanazawa 920-1192, Japan
Hiroki Kotaka
Elements Strategy Initiative for Catalysts and Batteries (ESICB), Kyoto University, Kyoto 615-8245, Japan
Fumiyuki Ishii‡
Nanomaterials Research Institute, Kanazawa University, Kanazawa 920-1192, Japan

(Received 9 January 2018; Accepted 29 October 2018; Published 24 November 2018)

We investigate the effect of the electric field on the edge states in one-bilayer Bi(111) by first-principles calculations. We calculate the band structures of armchair and zigzag Bi nanoribbons. With increasing strength of the electric field \( E > 2.1 \) V/A, the armchair nanoribbon shows a topological phase transition from non-trivial metallic edge states to insulating edge states. However, under the same conditions, the zigzag nanoribbon shows a topological phase transition from non-trivial metallic edge states to trivial metallic edge states. We expect that these findings will contribute to the development of, e.g., spin current switches for use in next-generation devices.

Keywords: Bismuth; Topological insulator; Edge states; Density functional theory

I. INTRODUCTION

A topological insulator behaves as an insulating material in its bulk, but can conduct electrons along its surface. This behavior results from non-trivial metallic edge states due to its non-trivial topology being different from vacuum [1-3]. The origin of this non-trivial topology is band inversion induced by strong spin-orbit interactions; thus, many Bi alloys have been reported to be topological insulators [4-9].

One-bilayer Bi(111) is a typical two-dimensional topological insulating material. It has been theoretically predicted that Bi(111) is a topological insulator [10, 11] and films of this material have been experimentally formed on Si(111) substrates [12, 13]. In addition, non-trivial edge states have been observed in Bi(111) formed on Bi2Te3 substrates [14]. Zigzag nanoribbons of one-bilayer Bi(111) show a pair of spin-degenerate bands originating from both edges. These bands are split by an electric field of \( E = 1.0 \) V/A [15]. These non-trivial edge states are stable at an electric field \( E < 0.8 \) V/A [16].

Controlling spin currents on a topological insulator using an electric field expands the possibilities of using these materials for preparing novel devices [17]. In addition, as the non-trivial metallic edge states in topological insulators have dissipation-free spin currents, they could allow the development of spin current switches for use in next-generation devices [18]. In our previous study, we demonstrated that a topological phase of one-bilayer Bi(111) could be switched using an electric field of 2.1 V/A, which was predicted by computing the topological invariant of the bulk system.

In this study, we investigated the band structures of Bi(111) nanoribbons under an electric field by first-principles calculations and confirmed a topological phase transition from non-trivial edge states to trivial edge states. Using fully relativistic density functional calculations, we calculated the band structures in both armchair Bi nanoribbon (ABNR) and zigzag Bi nanoribbon (ZBNR) structures under an applied electric field. Analyzing the edge states in both nanoribbons upon application of a strong electric field, we observed that the non-trivial metallic edge states of ABNR changed to insulating states, whereas the non-trivial metallic edge states of ZBNR changed to trivial metallic edge states.

II. METHOD

Figure 1 shows the unit cell of one-bilayer Bi(111) structure where the direction of the applied electric field is indicated. We used an in-plane lattice constant of 4.54 Å and buckling height of 1.45 Å, following a previous report of experimentally determined values [12]. Using OpenMX...
FIG. 2. The atomic structure and lattice vector of the (a) armchair nanoribbon and (c) zigzag nanoribbon used in this study. The edge atoms Bi1 and Bi2 are shown in (b) and (d), respectively. The width of a Bi nanoribbon is defined by \( N \) in (a) and (c) for the armchair nanoribbon and the zigzag nanoribbon, respectively, where \( N \) is the number of buckled Bi dimer lines.

FIG. 3. (a) Band structures of the armchair nanoribbon at \( E = 1.0 \text{ V/Å} \). The blue lines indicate the band contribution from atoms inside the nanoribbons. The blue circles indicate the intersections of the Fermi level and band edges. (b) Partial density of states of edge atoms. Bi1 and Bi2 correspond to the edge atoms shown in Fig. 2(b). (c) Partial density of states of the upper and lower atoms inside the nanoribbons.

FIG. 4. (a) Band structures of the armchair nanoribbon at \( E = 4.0 \text{ V/Å} \). The blue lines indicate the band contribution from atoms inside the nanoribbons. (b) Partial density of states of edge atoms. Bi1 and Bi2 correspond to the edge atoms shown in Fig. 2(b). (c) Partial density of states of the upper and lower atoms inside the nanoribbons.

code [19], we performed fully relativistic density functional calculations for both ABNR and ZBNR structures. We used a local spin density approximation as an exchange correlation functional [20], norm-conserved pseudopotentials [21], and the linear combination of multiple pseudo-atomic orbitals for wave function expansion [22, 23]. Spin-orbit interactions were considered using the fully relativistic total angular momentum \( j \)-dependent pseudopotentials [21]. The cutoff radius was 8.0 Bohr radius and pseudo-atomic orbitals were specified as s3p3d2 (i.e., three s-orbitals, three p-orbitals, and two d-orbitals). An energy cutoff of 300 Ry was used, with \( k \)-space sampling points of 128 \( \times \) 1 \( \times \) 1 for the reciprocal lattice vectors. The electric field was introduced as a saw-tooth potential [24, 25]. We did not consider changes in the lattice parameters and atomic positions induced by the electric field.

We considered Bi nanoribbon structures in the model in order to investigate the topological phase transition induced by an electric field. Figure 2(a, b) shows the ABNR and ZBNR structures used in this study. The number of Bi atoms in the unit cell of ABNR and ZBNR was 128 and 64, respectively. The width of the ABNR and ZBNR was given by \( N = 64 \) and 32, respectively, where \( N \) is the number of buckled Bi dimer lines, as shown in Figs. 2(a) and 2(c), respectively. The widths of ABNR and ZBNR in this study corresponded to 143.01 Å and 145.28 Å, respectively [26]. Lattice vectors \( a, b, \) and \( c \) were defined, where the vacuum space was 30 Å and 20 Å in the \( b \) and \( c \) directions, respectively, in both systems.
To distinguish non-trivial edge states from trivial edge states, we counted the intersections between the Fermi level and edge bands. Topological insulators have gapless non-trivial edge states, which connect the conduction and valence bands, where each spin-resolved edge band crosses the Fermi level an odd number of times in the half Brillouin zone [27]. Hence, if the number of intersections divided by the number of edges (two) was odd, the system was non-trivial.

III. RESULTS AND DISCUSSION

Figures 3(a) and 4(a) show the electric-field dependence of the ABNR band structure, where the blue lines indicate the band contribution from atoms inside the nanoribbon. Figures 3(b) and 4(b) show the partial density of states (PDOS) projected on edge atoms [Bi1 and Bi2 shown in Fig. 2(b)], while Figs. 3(c) and 4(c) show the PDOS of the atoms inside the nanoribbon. We concluded that the bands around the Fermi level were mainly composed of edge states. The bands around the Fermi level were divided by the number of edges (two) was odd, the system was non-trivial.

In the case of the band structure at $E = 1.0 \text{ V/Å}$, the edge states were non-trivial as two degenerated edge bands intersected the Fermi level once between the $\Gamma$ and $X$ points. On the other hand, as shown in Fig. 6(b), at $E = 4.0 \text{ V/Å}$ trivial edge states were observed as two edge bands intersected the Fermi level eight times between the $\Gamma$ and $X$ points, i.e., the edge states for each edge intersected the Fermi level four times.

We found that the non-trivial edge states of both ABNR and ZBNR could be switched to trivial edge states by applying an electric field of $4.0 \text{ V/Å}$; the ABNR switched from metallic to insulating behavior, while ZBNR remained metallic. A previous first-principles study revealed the existence of non-trivial edge states in ABNR and ZBNR without an electric field [11]. In the case of ZBNR, it was reported that the non-trivial edge states existed even under an applied electric field $E < 1.0 \text{ V/Å}$ [15, 16]. Our results corresponded with those of our previous study of a bulk system where one-bilayer Bi(111) showed a topological phase transition with an electric field $E > 2.1 \text{ V/Å}$ [18]. It is interesting that the two nanoribbon structures showed different edge

![Figure 5](image1.png)

![Figure 6](image2.png)
states under a high electric field, resulting in only the ABNR showing the metal-insulator transition, while the ZBNR remained metallic. Such behavior is reminiscent of the electronic structure of graphene nanoribbons. In the case of hydrogenated graphene nanoribbons, the armchair nanoribbon has a bandgap, whereas the zigzag nanoribbon has flat metallic edge states [28, 29].

Generally, the topological phase transition is induced by band inversion. The origin of the topological insulating phase of one-bilayer Bi(111) is band inversion originating from strong spin-orbit interactions [10]. Under an applied electric field, further band inversion occurs and the system returns to the trivial insulating phase [18]. The origin of this band inversion is charge transfer between upper and lower Bi atoms in Fig. 1(b). In our calculations of the Bi nanoribbon, similar band inversion occurred in bulk-like states. In Figs. 3(c) and 5(d), the PDOS of the upper atom was larger than that of the lower atom of the valence band near the Fermi level. In Figs. 4(c) and 6(d), the PDOS of the lower atom was larger than that of the upper atom of the valence band near the Fermi level.

IV. CONCLUSION

We calculated the band structures of armchair and zigzag nanoribbons in one-bilayer Bi(111) and analyzed the edge states in order to investigate the topological phase transition induced by an electric field. The initial non-trivial edge states of both nanoribbons disappeared under an applied electric field. These results are consistent with those of one-bilayer Bi(111) showing a topological phase transition under an electric field of 2.1 V/Å confirmed by computing a $\nu_2$ topological invariant for the bulk [18]. When increasing the electric field strength up to $E = 4.0$ V/Å, the ABNR showed a transition from non-trivial metallic edge states to trivial insulating states, whereas ZBNR showed a transition from non-trivial to trivial metallic edge states. These findings are expected to contribute to a better understanding of the behavior of Bi nanostructures, which may assist in the development of novel devices using this material. These findings show that ZBNR structures are suitable for devices switching between charge current and spin current, while the ABNR structures are suitable for switching spin currents.

ACKNOWLEDGMENTS

This work was supported by Grant-in-Aid for Scientific Research on Innovative Area, “Nano Spin Conversion Science” (Grant No. 17H05180). This work was also supported by JSPS Grant-in-Aid for Scientific Research on Innovative Areas, “Discrete Geometric Analysis for Materials Design” (Grant No. 18H04481). The work was partially supported by Grants-in-Aid on Scientific Research under Grant No. 16K04875 from Japan Society for the Promotion of Science. The computations in this research were performed using the supercomputers at RIIT, Kyushu University, and the ISSP, University of Tokyo.

[1] C. L. Kane and E. J. Mele, Phys. Rev. Lett. 95, 146802 (2005).
[2] L. Fu and C. L. Kane, Phys. Rev. B 74, 195312 (2006).
[3] M. Z. Hasan and C. L. Kane, Rev. Mod. Phys. 82, 3045 (2010).
[4] J. C. Y. Teo, L. Fu, and C. L. Kane, Phys. Rev. B 78, 045426 (2008).
[5] D. Hsieh, D. Qian, L. Wray, Y. Xia, Y. S. Hor, R. J. Cava, and M. Z. Hasan, Nature 452, 970 (2008).
[6] H. Zhang, C.-X. Liu, X.-L. Qi, X. Dai, Z. Fang, and S.-C. Zhang, Nat. Phys. 5, 438 (2009).
[7] Y. Xia, D. Qian, D. Hsieh, L. Wray, A. Pal, H. Lin, A. Bansil, D. Grauer, Y. S. Hor, R. J. Cava, and M. Z. Hasan, Nat. Phys. 5, 398 (2009).
[8] Y. L. Chen, J. G. Analytis, J.-H. Chu, Z. K. Liu, S.-K. Mo, X. L. Qi, H. J. Zhang, D. H. Lu, X. Dai, Z. Fang, S. C. Zhang, I. R. Fisher, Z. Hussain, and Z.-X. Shen, Science 325, 178 (2009).
[9] D. Xiao, Y. Yao, W. Feng, J. Wen, W. Zhu, X.-Q. Chen, G. M. Stocks, and Z. Zhang, Phys. Rev. Lett. 105, 096404 (2010).
[10] S. Murakami, Phys. Rev. Lett. 97, 236805 (2006).
[11] M. Wada, S. Murakami, F. Freimuth, and G. Bihlmayer, Phys. Rev. B 83, 121310 (2011).
[12] T. Nagao, J. T. Sadowski, M. Saito, S. Yaginuma, Y. Fujikawa, T. Kogure, T. Ohno, Y. Hasegawa, S. Hasegawa, and T. Sakurai, Phys. Rev. Lett. 93, 105501 (2004).
[13] S. Yaginuma, K. Nagaoka, T. Nagao, G. Bihlmayer, Y. M. Koroteev, E. V. Chulkov, and T. Nakayama, J. Phys. Soc. Jpn. 77, 014701 (2008).
[14] T. Hirahara, G. Bihlmayer, Y. Sakamoto, M. Yamada, H. Miyazaki, S.-i. Kimura, S. Blügel, and S. Hasegawa, Phys. Rev. Lett. 107, 166801 (2011).
[15] H. Kotaka, F. Ishii, M. Saito, T. Nagao, and S. Yaginuma, Jpn. J. Appl. Phys. 51, 025201 (2012).
[16] L. Chen, Z. F. Wang, and F. Liu, Phys. Rev. B 87, 235423 (2013).
[17] Q. Liu, X. Zhang, L. Abdalla, A. Fazzio, and A. Zunger, Nano Lett. 15, 1222 (2015).
[18] H. Sawahata, N. Yamaguchi, H. Kotaka, and F. Ishii, Jpn. J. Appl. Phys. 57, 030309 (2018).
[19] T. Ozaki et al., http://www.openmx-square.org/.
[20] J. P. Perdew and A. Zunger, Phys. Rev. B 23, 5048 (1981).
[21] G. Theurich and N. A. Hill, Phys. Rev. B 64, 073106 (2001).
[22] T. Ozaki, Phys. Rev. B 87, 155108 (2003).
[23] T. Ozaki and H. Kino, Phys. Rev. B 69, 195113 (2004).
[24] K. Kunc and R. Resta, Phys. Rev. Lett. 51, 686 (1983).
[25] R. Resta and K. Kunc, Phys. Rev. B 34, 7146 (1986).
[26] The width of ABNR (ZBNR) can be calculated by (N − 1)/2 × 4.54 Å (N × 4.54 Å).
[27] L. Fu and C. L. Kane, Phys. Rev. B 76, 045302 (2007).
[28] M. Fujita, K. Wakabayashi, K. Nakada, and K. Kusakabe, J. Phys. Soc. Jpn. 65, 1920 (1996).
[29] K. Nakada, M. Fujita, G. Dresselhaus, and M. S. Dresselhaus, Phys. Rev. B 54, 17954 (1996).