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Cs$_2$NaGaBr$_6$: a new lead-free and direct band gap halide double perovskite

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In this work, we have studied new double perovskite materials, A$_2$$^{1+}$B$_2$$^{2+}$X$_6$$^{1–}$, where A$_2$$^{1+}$ = Cs, B$_2$$^{2+}$ = Li, Na, B$_3$s = Al, Ga, In, and X$_6$$^{1–}$ = I, Br. We used the all electron full-potential linearized augmented plane wave (FP-LAPW+lo) method within the framework of density functional theory. We used the mBJ approximation and WC-GGA as exchange–correlation functionals. We optimized the lattice constants with WC-GGA. Band structures were calculated with and without spin–orbit coupling (SOC). Further, band structures for Cs$_2$LiGaBr$_6$ and Cs$_2$NaGaBr$_6$ were calculated with SOC + mBJ to correct the band gap values with respect to experimental value. We obtained direct bandgaps at Γ-point of 1.966 eV for Cs$_2$LiGaBr$_6$ and 1.762 eV for Cs$_2$NaGaBr$_6$, which are similar to the parent organic–inorganic perovskite (MAPI) CH$_3$NH$_3$PbI$_3$ (E$_g$ = 1.6 eV). Total and partial density of states were analyzed to understand the orbital contribution of Cs, Na, Li, Ga and Br near the Fermi level. The optical properties in terms of real and imaginary ϵ, refractive index n, extinction coefficient k, optical conduction ϵ, absorption l, and reflectivity R were calculated. A study of the elastic and mechanical properties shows that both materials are thermodynamically stable. A stable, direct bandgap and a gap value close to those of MAPI make Cs$_2$NaGaBr$_6$ a great competitor in the Pb-free hybrid perovskite solar cells world.

1. Introduction

The inevitable crisis in energy and climate change associated with conventional fossil fuel usage needs renewable energy technologies to be created. The organic–inorganic hybrid halide perovskites CH$_3$NH$_3$PbX$_3$ (where X = I, Cl, Br) have attracted much attention in high-efficiency solar cell applications, solar fuel generation and solar hydrogen production. However, the poor stability and toxicity due to Pb (lead) have limited their commercialization on a large scale, which makes it necessary to search for Pb-free and stable new materials as alternatives. Dual halides of perovskite have stimulated great attention.

The double-perovskite halides are a large family of quaternary halides. The vast geometrical range of these materials poses opportunities to find new solar and optoelectronic materials; however, it also raises challenges in testing a large number of compounds to classify the most promising with ideal energetic, structural and electronic properties for solar cell applications. A series of double-perovskite halide compounds such as Cs$_2$AgBiCl$_6$ and Cs$_2$AgBiBr$_6$ have recently attracted considerable interest as promising alternatives to the CH$_3$NH$_3$PbI$_3$ solar absorber material because they are Pb-free and have improved stability. Dan and co-worker predicted thermodynamic stability of a number of double-perovskite halides using density functional theory (DFT). All inorganic double perovskite material shows much attention to replace lead based perovskite material due to their three dimensionality and non toxic nature. Recently, Giustino and Snaith, predict new elements forming halide double perovskites. We are choosing one class of these materials from there proposed materials, see Fig. 1a, except F (due to large bandgap) and I (due to instability) as A$_2$$^{1+}$B$_2$$^{2+}$X$_6$$^{1–}$.

In this context, we investigate the stable and direct bandgap double perovskite material A$_2$$^{1+}$B$_2$$^{2+}$X$_6$$^{1–}$, where A$_2$$^{1+}$ = Cs, B$_2$$^{2+}$ = Li, Na, B$_3$s = Al, Ga, In, and X$_6$$^{1–}$ = I, Br, see Fig. 1b. We will study structural as well as electronic properties of these materials and deeply analyzed optical and thermodynamic properties of selected materials which lies close to the bandgap of CH$_3$NH$_3$PbI$_3$.

2. Computational details

Our computational calculations are based on density functional theory (DFT), using the full-potential linearized augmented plane wave plus local orbitals (FP-LAPW+lo) method as embedded in the WIEN2k scientific code. We employed more accurate exchange–correlation potential flavor as generalized gradient approximation (WC-GGA) for the calculation of the
structural, electronic and thermodynamic properties. In addition, for obtaining accurate bandgap, we also applied the modified Becke–Johnson (mBJ)\textsuperscript{20,21} schemes over the WC-GGA. In the past, the mBJ scheme yields promising electronic band structures and bandgap values for lead halide perovskites and various types of semiconductors compare to experimental values.\textsuperscript{22–24} In this paper we demonstrate that mBJ over WC-GGA give results close to experimental one for Cs\textsubscript{2}AgBiCl\textsubscript{6} and than applied to predicted A\textsuperscript{2+}B\textsuperscript{2+}B\textsuperscript{3+}X\textsuperscript{6−} compounds. We use experimental lattice parameter of Cs\textsubscript{2}− and Na-based, as shown in Fig. 1a. First of all, structural parameters like lattice constant and bulk modulus are obtained by minimizing the total energy versus volume for A\textsuperscript{2+}B\textsuperscript{2+}B\textsuperscript{3+}X\textsuperscript{6−}. Electronic calculations have been performed with k-mesh of 13 × 13 × 13 and finer k-mesh of 24 × 24 × 24 for calculating the optical properties. All structures were optimized with energy convergence tolerance of 10−5 Ryd.

3. Results and discussion

3.1 Structural properties

According to proposed plan of study the prospective view of crystal structure of possible double perovskites A\textsubscript{2+}B\textsuperscript{2+}B\textsuperscript{3+}X\textsuperscript{6−} where A\textsubscript{2+} = Cs, B\textsuperscript{2+} = Li, Na, B\textsuperscript{3+} = Al, Ga, In and X\textsuperscript{6−} = Cl, Br, is shown in Fig. 1b. For simplicity, we categorized all 12 possible compounds into two categories, one is Li-based and second is Na-based, as shown in Fig. 1a. First of all, structural parameters like lattice constant and bulk modulus are obtained by minimizing the total energy versus volume for A\textsuperscript{2+}B\textsuperscript{2+}B\textsuperscript{3+}X\textsuperscript{6−} compounds. We use experimental lattice parameter of Cs\textsubscript{2}AgBiCl\textsubscript{6} (ref. 16) as our starting point. The Birch–Murnaghan’s equation of states\textsuperscript{25} is used for optimization of structural parameters of these compounds are listed in Table 1.

Optimized lattice constants for all studied compounds are between 9.8 Å to 10.97 Å which are quite close to experimentally synthesized double perovskites like Cs\textsubscript{2}AgBiCl\textsubscript{6} (10.77 Å) and Cs\textsubscript{2}AgBiBr\textsubscript{6} (11.27 Å).\textsuperscript{16}

The optimized bulk modulus (B) for Cs\textsubscript{2}LiAlCl\textsubscript{6} is 39.58 GPa which is highest among all other compounds. In contrast, Cs\textsubscript{2}LiInBr\textsubscript{6} has smallest value of B is 20.45 GPa which shows the hardness of these double perovskites. There is no theoretical or experimental data available for comparison of these optimized compounds.

After optimizing the lattice constants, it is important to characterize these compounds on the basis of band gap values, which are close to the best hybrid organic–inorganic perovskites.

3.2 Electronic band structure

To study about the electronic behavior of materials, band structure plays very important role. The electronic nature of materials can be disclosed using band structure such as metallic or semiconducting etc. Physical properties of solids such as electrical resistivity and optical behavior, can be explain successfully from electronic band structure and forms a foundation for solid state devices (transistors, solar cells, etc.). Therefore, band structure is calculated to realize electronic behavior of all Cs\textsubscript{2}LiB\textsuperscript{3+}X\textsuperscript{6−} and Cs\textsubscript{2}NaB\textsuperscript{3+}X\textsuperscript{6−} compounds where B\textsuperscript{3+} = Al, Ga, In and X\textsuperscript{6−} = Cl, Br. We can calculate band gap for all studied compounds with three different ways. First, band gap obtained by simple scf calculated where we did not incorporate spin–orbit coupling (SOC). Second one is to incorporate spin–orbit coupling to find the band gap values close to experimental values. Also we find splitting of band near the valence band maxima (VBM) or conduction band minima (CBM). Third, even if we could not match our bandgap values with experimental, we use different method to correct the band gap. Here we use mBJ method, which is quite expensive calculation with respect to time taken by CPU’s in computational.

For our compounds, the calculated band gap of all materials without SOC and mBJ + SOC are given in Table 1. Clearly we can see, that only Cs\textsubscript{2}LiGaBr\textsubscript{6} and Cs\textsubscript{2}NaGaBr\textsubscript{6} have small band gap, 0.731 eV and 0.451 eV respectively. While all other compounds have band gap above 1.4 eV without SOC and mBJ + SOC. We observe in double perovskite materials Cs\textsubscript{2}AgBiCl\textsubscript{6} and Cs\textsubscript{2}AgBiBr\textsubscript{6} (as a test calculation) have band gap 2.77 eV and 2.19 eV respectively.\textsuperscript{16} Which we reproduced by WIEN2k and for Cs\textsubscript{2}AgBiCl\textsubscript{6} case, we find band gap values for without SOC and with SOC, mBJ and mBJ + SOC, and values are 1.702 eV, 1.629 eV, 3.088 eV and 2.66 eV respectively. Also for Cs\textsubscript{2}AgBiBr\textsubscript{6}, without SOC (1.16 eV), with SOC (1.163 eV), mBJ (2.165 eV) and mBJ + SOC (1.947 eV). These results clearly shows that in double

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**Fig. 1** (a) Possible combination of A\textsuperscript{2+}B\textsuperscript{2+}B\textsuperscript{3+}X\textsuperscript{6−} and (b) prospective view of double perovskites crystal structures A\textsuperscript{2+}B\textsuperscript{2+}B\textsuperscript{3+}X\textsuperscript{6−}, where A\textsubscript{2+} = Cs, B\textsuperscript{2+} = Li, Na, B\textsuperscript{3+} = Al, Ga, In and X\textsuperscript{6−} = Cl, Br.
perovskites, WIEN2k underestimate the band gap values substantially until we incorporate mBJ + SOC. So our target is to find new Pb free material, whose band gap is close to 1.6 eV to replace CH₃NH₃PbI₃ at room temperature.

We concluded by analyzing Table 1, that if we apply mBJ + SOC on material whose band gap is already above 1.4 eV, results in larger band gap value probably >2 eV. So we decided two candidates remaining, Cs₂LiGaBr₆ (0.731 eV) and Cs₂NaGaBr₆ (0.451 eV).

We extend our further study only focusing these two materials. We calculated band gap for Cs₂LiGaBr₆ with and without SOC. The band structures are given in Fig. 2a. The band gap values for Cs₂LiGaBr₆ with and without SOC are 0.731 eV (red color) and 0.646 eV (blue color) respectively. Which indicate the importance of SOC in Cs₂LiGaBr₆, SOC slightly decrease in band gap value (see Fig. 2a), we can see that spin–orbit coupling splitting VBM in majority, while a minor splitting around 2 eV in CBM.

On the other hand in case of Cs₂NaGaBr₆, the band gap value, without spin–orbit coupling (0.45 eV) and decreasing with spin–orbit coupling (0.38 eV), (see Fig. 2b). Also if we examine the Fig. 2b more closely, we can see that VBM is splitting near Fermi energy at Γ point as well as SOC shifting CBM towards Fermi level. However, the SOC effect is spread over whole band structure in VBM too. Next we calculated the band structure of Cs₂LiGaBr₆ and Cs₂NaGaBr₆ with mBJ + SOC, shown in Fig. 3a and b. The calculated direct band gap values for Cs₂LiGaBr₆ and Cs₂NaGaBr₆ are 1.966 eV and 1.76 eV, respectively.

Among these two final materials Cs₂NaGaBr₆ and Cs₂LiGaBr₆ band gap values are more close to the experimental value of CH₃NH₃PbI₃ (Cl, Br). As we know that a band gap between 1.0 and 1.7 eV, electrons can be released without creating too much heat and makes an effective solar semiconductor in this range. The photon energy of light varies according to the different wavelengths of light. However, the nature of band gaps of these compounds were indirect. While recently studied double perovskites have direct band gap but band gap values are beyond this range and some have band gap values in effective range but nature of band gap were indirect, which is not ideal for applications in solar cell.

A high carrier mobility is strongly desirable for competent electronic and optoelectronic devices. The effective masses of MAPI are <0.2 mₑ and the carrier mobility of <100 cm² V⁻¹ s⁻¹ is moderate in comparison to conventional semiconductors such as Si or GaAs (>1000 cm² V⁻¹ s⁻¹). The balanced effective mass in MAPI may lead to ambipolar conductivity in perovskite solar cells, which facilitates the p-
3.4 Optical properties

The linear optical properties are described using the frequency-dependent dielectric\(\varepsilon(\omega) = \varepsilon_0 + i\varepsilon_2(\omega)\) function. The equation of frequency-dependent imaginary part of dielectric function \(\varepsilon_2(\omega)\) for cubic crystal is provided as:\(^{18}\)

\[
\varepsilon_2(\omega) = \frac{8}{\pi^2\varepsilon_0^2} \int_{-\infty}^{\infty} -\frac{P(x)}{\omega\omega_0^2}\omega_0\mathrm{d}\omega
\]

where \(P(x)\) is the dipole momentum matrix of the exterior band transformation. The joint DOS and transition momentum matrix components heavily correlate the dielectric feature \(\varepsilon_2(\omega)\).

The real part of the dielectric function \(\varepsilon_1(\omega)\) can be acquired from the \(\varepsilon_2(\omega)\) relationship provided in ref. 39 by Kramers-Kronig.

\[
\varepsilon_1(\omega) = \frac{2}{\pi} \int_{0}^{\infty} \frac{\omega\varepsilon_2(\omega)}{\omega^2 - \omega_0^2}\mathrm{d}\omega
\]

By dispersing real and imaginary components of dielectric features, other optical parameters such as refractive indices, reflectivity, optical conductivity, absorption coefficient and so on can be calculated. \(Cs_2LiGaBr_6\) and \(Cs_2NaGaBr_6\)’s linear optical characteristics were investigated by calculating the optical parameters, dielectric constant \(\varepsilon_0(\omega)\), refractive index \(n(\omega)\), extinction coefficient \(k(\omega)\), absorption coefficient \(I(\omega)\), reflectivity \(R(\omega)\), and optical conductivity \(\sigma(\omega)\) shown in Fig. 6. The static dielectric constant \(\varepsilon_1(0)\) is 1.6 eV for \(Cs_2LiGaBr_6\) and 1.7 eV for \(Cs_2NaGaBr_6\) without any contribution from the lattice vibration.

The complex refractive index as a function of energy in eV is shown in Fig. 6. The real part of refractive index \(n\) is a measure of phase velocity in a medium of electromagnetic (EM) wave and imaginary part \(k\) control the effect of EM wave traveling through a material. The calculated static refractive index \(n(0)\) are around ~1.8 for both materials while the highest values of \(n(\omega)\) and \(k(\omega)\) for \(Cs_2LiGaBr_6\) are 3.0 eV and 3.25 eV respectively. In case of \(Cs_2NaGaBr_6\) these values are 2.5 eV and 3.5 eV for \(n(\omega)\) and \(k(\omega)\). The optical conductivity corresponds to the conduction of electrons produced when a photon of a certain frequency is incident upon a material.

Fig. 3 The calculated band structure of (a) \(Cs_2LiGaBr_6\) and (b) \(Cs_2NaGaBr_6\) with modified band gap using mBJ + SOC scheme.
[Ω cm]⁻¹ at 3.4 eV. While for Cs₂NaGaBr₆ first peak of 915 [Ω cm]⁻¹ at 3.6 eV and maximum (σ) of 6015 [Ω cm]⁻¹ at 9.2 eV. Cs₂NaGaBr₆ has high optical conductivity in the visible light region (1.65–3.1 eV), which is important for solar cell materials. The solar energy conversion efficiency determines from absorption coefficient and it indicates how far light of a specific frequency can penetrate into the material before absorption. The absorption coefficient spectrum f(ω), started at 1.96 eV and its maximum arises at 3.26 eV (380.32 nm) for Cs₂LiGaBr₆ and for Cs₂NaGaBr₆ its started from 1.76 eV and it maxima arises at 3.72 eV (333.29 nm). The absorption coefficient values rapidly increases when the incident photon energy reaches the absorption edge. But at the other side, in the high-energy zone, the absorption coefficients are rapidly decreasing and this is a typical feature of semiconductors. In visible region Cs₂NaGaBr₆ has more absorption that Li-based Cs₂LiGaBr₆. While maximum of reflectivity R(ω) is at about 2.89 eV for Cs₂LiGaBr₆ and for Cs₂NaGaBr₆ (0.13 or 13%) at 2.54 eV.

3.5 Elastic and mechanical properties

The effective elastic constants provide an appropriate description of materials for desirable practical applications. The elastic constants describe the structure stability and response of the materials to external forces.

The calculated elastic constants for Cs₂LiGaBr₆ and Cs₂NaGaBr₆ are presented in Table 2. No experimental results are available for comparison to our predicted values. The Born stability criteria for cubic crystals i.e., C₁₁ + 2C₁₂ > 0, C₁₁ − C₁₂ > 0, C₁₁ > 0, C₄₄ > 0 and C₁₂ < B < C₁₁ are fulfilled by these
materials. This justified that these materials are elastically stable against deforming force.

Further, elastic constants are used to calculate the important mechanical properties of materials under study using standard relations\textsuperscript{41,42} and presented in Table 2.

The shear modulus \( G_H \) is the arithmetic mean of the \( G_R \) and \( G_H \) shear moduli measure the plastic deformation of the material to applied stress. The higher value of \( G_H \) and Young modulus \( Y \) of Cs\(_2\)LiGaBr\(_6\) indicate that this material offer more resistance to plastic deformation and hence stiffer than Cs\(_2\)NaGaBr\(_6\). Pugh\textsuperscript{43} \((B/G)\) reflect the brittle and ductile behavior of materials. It is clear from the Table 2 that \( B/G \) ratio for both materials is less than critical value of 1.75, hence both materials show brittle nature. The negative/positive value of Cauchy’s pressure \((C'' = C_{12} - C_{44})\) also indicate the brittle/ductile behavior of materials. The negative value of Cauchy’s pressure (Table 2) further confirm the brittle behavior of Cs\(_2\)LiGaBr\(_6\) and Cs\(_2\)NaGaBr\(_6\). Poisson’s ratio \( \nu \) measures the stability of a crystal against compressibility. The smaller value of Poisson’s ratio indicate that these materials is relatively stable against shear stress. The calculated values of anisotropic factor for Cs\(_2\)LiGaBr\(_6\) and Cs\(_2\)NaGaBr\(_6\) are given in Table 2. The deviation of \( A \) from unity measure the degree of anisotropy of material. It is evident from the table that anisotropic factor is greater than unity, hence their properties vary in different crystallographic directions. Shear constant or tetragonal shear modulus \( C' \) define the dynamical stability of materials. It also describes the stability to tetragonal distortion. For dynamical stability \( C' > 0.44\). The positive value of \( C' \) for the materials under investigation (Table 2) predicted that these materials are mechanically stable.

Fig. 5 Calculated (a) total and (b) partial DOS of Cs\(_2\)NaGaBr\(_6\).
4. Conclusion

In this study, double perovskites $A_2^{+1}B^{2+}B'^{3+}X_6^{1-}$, where $A_2^{+1} = Cs, B^{2+} = Li,Na, B'^{3+} = Al, Ga, In$ have been investigated using all-electron full potential linearized augmented plane wave (FP-LAPW+lo) method within the framework of density functional theory. We optimize all materials using WC-GGA approximation along with band gaps. In addition to this, we employed modified Becke-Johnson band gap correction in order to obtain correct band gap values with respect to experimental material (CH$_3$NH$_3$PbI$_3$). After carefully optimizing, the volume optimization and predicted lattice constants of $A_2^{+1}B^{2+}B'^{3+}X_6^{1-}$ were obtained. We calculated band gap of these materials. Among these materials only Cs$_2$LiGaBr$_6$ and Cs$_2$NaGaBr$_6$ have band gap values 0.731 eV and 0.45 eV, respectively. Rest of materials have band gap above 1.4 eV, which may further increase over 2 eV on applying mBJ correction. We also study the effect of spin–orbit coupling (SOC) in these materials. We found that SOC effect is only lowering the bands in energies. Due to spin–orbit coupling, band gap values are reduced from 0.731 to 0.646 eV for Cs$_2$LiGaBr$_6$ and from 0.45 to 0.38 eV for Cs$_2$NaGaBr$_6$. Total density of state shows that Br is major contributor in valence band maxima and Ga contributes in conduction band minima. While in partial density of state (PDOS) reveal that Br-p orbital bands are contributing while Ga s-orbital. We have calculated optical spectra to study absorption for Cs$_2$NaGaBr$_6$ has more absorption coefficient than Cs$_2$LiGaBr$_6$. So we concluded that Cs$_2$NaGaBr$_6$ is more suitable candidate among studied double perovskite compounds on the basis of band gap value and optical absorption for solar cell application. Stable, direct band gap and value of gap close to MAPI makes Cs$_2$NaGaBr$_6$ a great competitor in Pb-free hybrid perovskite solar cell world. 

Table 2  The calculated values of elastic constants $C_{11}$, $C_{12}$ and $C_{44}$, Voigt’s shear modulus $G_V$, Reuss’s shear modulus $G_R$, Hill’s shear modulus $G_H$, $B/G$ ratio, Cauchy pressure ($C''$), Poisson’s ratio ($v$), anisotropy constant ($A$), and shear constant ($C'$) for Cs$_2$LiGaBr$_6$ and Cs$_2$NaGaBr$_6$.

| Comp.       | Cs$_2$LiGaBr$_6$ | Cs$_2$NaGaBr$_6$ |
|-------------|------------------|------------------|
| $C_{11}$    | 46.42            | 38.97            |
| $C_{12}$    | 19.48            | 14.16            |
| $C_{44}$    | 18.82            | 14.52            |
| $G_V$       | 17.20            | 13.68            |
| $G_R$       | 16.72            | 13.60            |
| $G_H$       | 16.96            | 13.64            |
| $Y$         | 42.85            | 34.10            |
| $B/G$       | 1.65             | 1.65             |
| $C''$       | −0.62            | −0.36            |
| $v$         | 0.25             | 0.25             |
| $A$         | 1.41             | 1.17             |
| $C'$        | 16.59            | 12.41            |

Fig. 6  Calculated optical properties of Cs$_2$LiGaBr$_6$ (dotted line) and Cs$_2$NaGaBr$_6$ (solid lines). (a) Optical constant ($n$, $k$), (b) optical conductivity $\sigma$, (c) absorption coefficient $I$ and (d) reflectivity $R$.

Conflicts of interest

There are no conflicts to declare.

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