Evaluation of different gravimetric methods to Moho recovery in Iran

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Abstract: The complexity of geological units in Iran because of several unique events like tectonics and orogenic activities in this region led to extensive investigations for Moho recovery by seismic methods therein. In this research, three gravimetric methods have been evaluated by some point-wise seismic data. We applied collocation method as an iterative process as well as modified forms of Sjöberg and Jeffrey’s theory of isostasy for local Moho depth recovery. The gravity data has been generated by GOCO03S model reduced by topography/bathymetry, sediment and consolidated crust effects. Although the iteration process in collocation approach only slightly changed the estimated depths, this method led to a better agreement with seismic data rather than others. Differences between collocation, Jeffrey and Sjöberg’s solutions with seismic studies are similar but Jeffrey and Sjöberg’s methods displayed a systematic bias. The standard deviations of the residuals among seismic data and gravimetric solutions are around 6 km. Overall, the evaluation of these approaches indicated that Moho from gravimetric approaches reduced only slightly the standard deviation of seismic Moho estimates. Significant discrepancies with seismic data have been detected in Makran subduction zone, Oman Sea, Persian Gulf and Caspian Sea. The explanation of such inconsistency can be partially due to the poor quality of CRUST1.0 data in these areas, as this model has been used to correct the gravity values that were input in the inversion procedures.

Keywords: Moho, Gravimetric inverse problem, Collocation, Isostasy, Seismic data
1. Introduction

The knowledge of the Mohorovičić discontinuity (Moho) can provide valuable information to understand some topical issues in solid Earth sciences (Sampietro, 2016). Its knowledge in the Iran block is one of the crucial issues in this region. Several unique events like tectonics and orogenic activities in Iran led to a complex geological structure of the area. Thus, it is important to study in deep the peculiar structure of the Iranian Moho applying different methods and different observations in order to have a comprehensive definition of its main features. Moho interface is commonly estimated by either seismic or gravimetric methods. Although seismic Moho estimates have a significant accuracy (at the level of 1-2 km), their coverage over entire of the Earth is quite poor. Thus, in regions where seismic data are sparse or missing, results of gravimetric studies can be profitably used. At global scale, this has been made possible after dedicated gravity-satellite missions, namely the Gravity Recovery and Climate Experiment (GRACE) (Tapley et al., 2004a, Tapley et al., 2004b) and the Gravity field and steady-state Ocean Circulation Explorer (GOCE) (Floberghagen et al., 2011). These two missions have provided global gravity field with an accuracy and a resolution which is suitable for investigating the Moho structure. Among successful seismic estimates, the early results dated back to Belousov et al. (1980). The most widely known crustal model based on seismic refraction is CRUST5.1 model (Mooney et al., 1998). Bassin et al. (2000) further upgraded it and called the new version, CRUST2.0. The CRUST1.0 (Laske et al., 2013) including ice layers, water, sediments and consolidated crustal layers, is the most recent version compiled with a 1×1 arc-deg spatial resolution. As already pointed out, because of insufficient seismic data coverage over large areas, gravimetric or combined gravimetric/seismic solutions have been utilized. Based on some isostasy hypotheses on compensating the Earth’s topographic masses, gravity data can be used to determine the Moho depth. Several basic theories were suggested to explain the mechanism of isostasy like those proposed by Pratt-Hayford (Pratt, 1855, Hayford, 1909) and Airy-Heiskanen (Airy, 1855, Heiskanen, 1931). Vening Meinesz (1931) modified the Airy-Heiskanen theory by considering a regional instead of a local compensation based on a thin plate lithospheric flexure model (Watts, 2001). Vening Meinesz theory had been modified by Parker (1973) in an iterative approach for Moho determination and Oldenburg (1974) made an attempt to stabilise this method by applying a low-pass filtering technique. The combination of these two methods was known as a Parker-Oldenburg method and it has been generalized for the 3-D gravity inversion by Gómez-Ortiz and Agarwal (2005) and Shin et al. (2007). Braitenberg et al. (2000) developed a similar method with integration of seismic data; also they estimated
variation of the Moho under the Tibet plateau by an iterative inversion method. Moritz (1990) improved the Vening Meinesz inverse problem for a global compensation by adopting the spherical approximation model of the Earth. Since there were some theoretical deficiencies in this isostatic method, Sjöberg (2009) reformulated Moritz’s theory and called it as the Vening Meinesz Moritz (VMM) problem. In this approach he solved a non-linear Fredholm’s integral equation of the first kind. Bagherbandi and Sjöberg (2012) made a comparison between the gravimetric VMM and local Airy-Heiskanen methods in the determination of Moho depth. Another approach based on the inversion of gravity data to determining the Moho depth is collocation method (Krarup, 1969, Tscherning, 1985, Moritz, 1990). Barzaghi et al. (1992) proposed an approach based on collocation principle, which propagate the covariance structure of the depth interface to the covariance function of the observed gravity field. Barzaghi et al. (2015) applied collocation method by combining the global gravity-gradient information of GOCE and local gravity data to Moho recovery. Barzaghi and Biagi (2014) implemented then a further version of the collocation method by including seismic Moho depths as input data. Braitenberg and Ebbing (2009) studied the structure of the crust by combination of GRACE and terrestrial gravity data. Some other scientists made attempt to estimate Moho depth by applying GOCE gravity gradient data (Braitenberg et al., 2010, Sampietro, 2011, Sampietro et al., 2014). Reguzzoni et al. (2013) combined seismic and GOCE data to obtain a new global Moho model. Tenzer et al. (2009, 2011, 2012a, 2012b) proved that applying the crustal density-contrast stripping corrections is appropriate for a gravimetric Moho recovery. They showed that gravitational contributions of topography and major known crustal density structures have a large spatial correlation with the Moho geometry.

In the area under investigation in this paper, several studies based on seismic data have been performed for the determination of the regional Moho model. Most of these studies concentrated on a specific area, for instance profiles between Shiraz-Mashhad, Tehran-Mashhad and Mashhad-Tabriz (Asudeh, 1982), the southern part of the Caspian Sea (Mangino and Priestley, 1998), Tehran region (Hatzfeld et al., 2003), Mashhad (Doloei and Roberts, 2003, Javan Doloei, 2003), Central Alborz and the northern Iran (Sodoudi et al., 2009, Radjaee et al., 2010), central Zagros (Paul et al., 2006, Shad Manaman et al., 2011), Kohe-Dagh (Nowrouzi et al., 2007), Naein (Nasrabadi et al., 2008), the northwest Iran (Taghizadeh-Farahmand et al., 2015), and Sanandaj-Sirjan zone (Sadidkhouy et al., 2012). Furthermore, based on terrestrial gravity data in this area with a quite homogenously coverage, Dehghani and Makris (1984) combined gravimetric and seismic data to determination of the crustal
structure of Iran. Abbazadeh et al. (2013) compared the effective elastic thickness of the lithosphere estimated by terrestrial and satellite data in Iran. Eshagh et al. (2017) reformulated two isostatic methods for Moho recovery by considering contributions of mean Moho over the whole Moho spectrum.

In this paper, we adopt collocation method as well as two isostatic approaches to determine the Moho depths inverting gravity data over Iran. The collocation inversion method for a two-layer model devised by Barzaghi and Biagi (2014) is applied. In addition, the generalized form of Jeffrey and Sjöberg’s method proposed by Eshagh et al. (2017) have been utilized in this study. These methods have been applied to gravity from GOCO03S gravitational model (Mayer-Gürr et al., 2012) reduced for the SRTM30_PLUS topographic/bathymetric data (Becker et al., 2009), the sediment and the crystalline data of CRUST1.0 (Laske et al., 2013). Comparisons of these Moho depth estimates have been finally performed with the seismic estimates available from literature.

2. The theoretical background

In this section, we review three gravimetric inversion methods that can be successfully applied to estimate the Moho depth. At first, we describe the procedure based on the collocation principle. Subsequently, we also discuss two alternative isostatic approaches, which are reformulations of Jeffrey and Sjöberg’s theories.

2.1 The collocation solution

The collocation method for Moho estimation is based on a stochastic approach derived from the Wiener filtering and prediction theory that allows estimating the signal correlated component based on the covariance structure of the data (Barzaghi and Biagi, 2014). In the years, it has been applied to determine the gravimetric estimate of the Moho (Barzaghi et al., 1992, Barzaghi and Biagi, 2014, Barzaghi et al., 2015). In this context, the covariance structure of the Moho depth is propagated to the covariance of the observed gravity in a simple two-layer model. In order to apply collocation for estimating the Moho depth, we should consider the following linear relationship which holds in planar approximation (Barzaghi and Biagi, 2014):
\[ \Delta g(x, y, 0) = G \iint dxdy \Delta \rho \frac{e T_0}{\left[T_0^2 + d_x^2\right]^{1/2}} \]

\( D_g \) is the Bouguer gravity anomaly minus its mean, \( G \) is the Newton’s gravitational constant, \( T_0 \) is the mean Moho depth, \( \varepsilon \) is the Moho depth undulation with respect \( T_0 \), \( \Delta \rho \) stands for the mean constant density contrast between the two layers and \( d_{xy} = \sqrt{x^2 + y^2} \).

Also, the following conditions must be fulfilled (Barzaghi and Biagi, 2014):

1) \( \varepsilon \) is a weak stationary stochastic process, ergodic in the mean and in the covariance

2) The noises in gravity and depth, \( n_g \) and \( n_h \) are spatially uncorrelated zero mean signals

3) The cross-correlations between signals and noises are zero

To perform the computation, the gravity auto-covariance and the cross-covariances between gravity and depth are needed, i.e.:

\[ C(D_g, D_g) = C_{DgDg} \left| \begin{bmatrix} P_i - P_j \end{bmatrix} \right| = C(D_g, D_g) \]

\[ C(e, D_g) = C_{eDg} \left| \begin{bmatrix} P_i - P_j \end{bmatrix} \right| = C(D_g, e) \]

Assuming that the observed gravity values contain a noise component, we can write:

\[ D_g^{OBS} = D_g + n_g \]

The collocation estimate of \( \varepsilon \) is (Moritz, 1980, Barzaghi et al., 1992, Barzaghi and Biagi, 2014):

\[ \hat{\varepsilon} = \left[ c_{Dg}^T C_{\varepsilon}^{-1} \right] \]

With

\[ c_{Dg} = C(e, D_g) , 1 = \left[ D_g^{OBS} \right] \text{ and } C_{\varepsilon} = \left[ C_{\varepsilon^{OBS}} \right] \]

As the first step to use this approach, the empirical covariance function of \( D_g^{OBS} \) should be estimated and modelled with appropriate positive definite model functions (Moritz, 1980). Under the hypotheses previously stated, the empirical covariance can be estimated as (Barzaghi et al., 1992):
\[
\hat{C}_{DgDg}(DP_k) = \frac{1}{N} \sum_{i=1}^{N} \frac{1}{N} \sum_{j=1}^{N} Dg_{OBS}(Q_i) Dg_{OBS}(Q_j)
\]

\[
P_{k-1} < |Q_i - Q_j| < P_k, \quad DP_k = P_k - P_{k-1}
\]

Also, auto and cross-covariance models must be defined in order to derive the estimator of \( \epsilon \) for Moho determination. One possible model for the auto covariance of \( Dg \) (see Barzaghi and Biagi (2014)) is:

\[
C_{Dg}(r) = \frac{A J_1(\alpha x)}{\alpha x} \quad (2-7)
\]

Where \( J_1(\cdot) \) is the first order Bessel function.

If this auto-covariance is considered, one can prove (Barzaghi et al., 1992) that:

\[
C_{\Delta g}(P,Q) = \frac{A}{2\pi G \rho a} \int \frac{dk e^{ikr} J_0(k|P - Q|)}{k} \quad (2-8)
\]

which can be evaluated by numerical integration methods.

The parameters \( A \) and \( \alpha \) are determined so that the model (2-7) fits the empirical estimated covariance values of \( Dg \). After deriving \( C_{Dg}(P,Q) \) by the expression above, we can then obtain \( \epsilon \) by applying formula (2-5). The final Moho estimate is then given as \( T = T_0 + \epsilon \).

Also, in order to refine the estimate, iterations on gravity residuals can be performed so that the final solution is obtained as \( T = T_0 + \epsilon_1 + ... + \epsilon_n \). Usually two or three iterations are computed.

### 2.2 The Jeffrey’s solution

Jeffrey (1976) has solved the problem of isostasy for Moho modelling in a very similar way to the VMM method (Sjöberg, 2009). Eshagh and Hussain (2016) proposed a different modelling of the isostatic gravity disturbance \( \delta g^I \) by considering the gravitational effects of topography and bathymetry, sediments and consolidated crystalline basement as follows:

\[
\delta g^I = \delta g - \delta g^{TB} - \delta g^S - \delta g^{Crys} + \delta g_C \quad (2-9)
\]
In this equation, $\delta g$ denotes the observed gravity disturbance which is the difference between measured and normal gravity at a computation point on the Earth, $\delta g_c$ is the compensation attraction, $\delta g^{TB}$ is the topographic/bathymetric effect on $\delta g$ , $\delta g^s$ and $\delta g^{crys}$ represent the gravitational effects of sediment and consolidated crust, respectively. Moritz (1990) and Sjöberg (2009) applied this equation as a fundamental condition to solve the VMM problem.

In order to define the compensation potential in equation (2-10), Eshagh et al. (2017) arranged the formula in Jeffrey (1976) in the following way:

$$V_c = G \iint_\sigma \int_{R-T_0}^{R-T_0-\varepsilon} \frac{\Delta \rho \rho'^2}{l} \, dr' \, d\sigma = G \sum_{n=0}^{\infty} \frac{\Delta \rho \Delta r}{(R-T_0)^{n+1}} \int_{R-T_0-\varepsilon}^{R-T_0} r'^{n+2} \, dr' P_n (\cos \psi) \, d\sigma \quad (2-10)$$

As stated before, $\varepsilon$ is the variation of the Moho depths relative to the mean value indicated by $T_0$. In this equation, $R$ is the radius of the Earth, $\sigma$ is the unit sphere, $r'$ denotes the geocentric distance of the infinitesimal mass element while $dr'$ and $d\sigma = \sin \theta d\theta d\lambda$ are the radial and the surface integration elements, $P_n (\cos \psi)$ is the Legendre polynomial of degree $n$ for the argument of the geocentric angle $\psi$. $\theta$ and $\lambda$ represent the spherical co-latitude and longitude of the element, $l$ is the Euclidean spatial distance which is a function of the $r'$ (see. Heiskanen and Moritz (1967)).

Further, Eshagh et al. (2017) solved the radial integral and expanded $\delta g_c$ in a spectral form according to the Heiskanen and Moritz (1967) scheme:

$$\left. \delta g_c \right|_{r=R} = GR \int_\sigma \left[ \Delta \rho \sum_{n=0}^{\infty} \frac{n+1}{n+3} \kappa^{n+3} \left[ 1 - \left( 1 - \frac{\varepsilon}{R-T_0} \right)^{n+3} \right] P_n (\cos \psi) \right] d\sigma \quad (2-11)$$

Where $\kappa = 1 - \frac{T_0}{R}$.

Also Eshagh et al. (2017) approximated the term $[ \varepsilon / (R-T_0)]^{n+3}$ by a binomial series and after simplification, (2-11) reduces to:

$$\delta g_c = \frac{GR}{R-T_0} \sum_{n=0}^{\infty} \left( n+1 \right) \kappa^{n+3} \int_\sigma (\Delta \rho \varepsilon) P_n (\cos \psi) \, d\sigma \quad (2-12)$$

They wrote this equation according to Laplacian harmonics of $\Delta \rho \varepsilon$ :

$$\delta g^{\varepsilon, \sigma} = 4\pi G \frac{n+1}{2n+1} \kappa^{n+2} (\Delta \rho \varepsilon) \quad (2-13)$$
By considering Eq. (2-9) and inserting (2-13) into that, they got:

\[
(\Delta \rho \epsilon)_n = -\frac{1}{4\pi G} \frac{2n+1}{n+1} \kappa^{-(n+2)} \left( \delta g_n - \delta g^T_B - \delta g^S - \delta g^C_{\text{cry}} \right)
\]

(2-14)

Eshagh et al. (2017) took the summation from both sides of Eq. (2-14) and extract \( \epsilon \) from the resulting expression and finally arrived at:

\[
\epsilon = -\frac{1}{4\pi G \Delta \rho} \sum_{n=0}^{\infty} \frac{2n+1}{n+1} \kappa^{-(n+2)} \left( \delta g_n - \delta g^T_B - \delta g^S - \delta g^C_{\text{cry}} \right)
\]

(2-15)

Since \( \epsilon \) is the undulation of Moho depths with respect to \( T_0 \), the total Moho depth is given as:

\[ T = T_0 + \epsilon. \]

### 2.3 The Sjöberg’s solution

The Vening Meinesz Moritz (VMM) inverse problem of isostasy (Sjöberg, 2009) has been developed and applied successfully over different areas of the Earth. The main difference between Jeffrey and Sjöberg’s method is how to write the compensation potential. Sjöberg (2009) used the compensation potential \( V_C \) derived by Moritz (1990):

\[
V_C = G\Delta \rho \int \frac{1}{r-n+1} P_n(\cos \psi) \left[ \int_{r-T}^{\infty} dT - \int_{r-T_0}^{r} dT' \right] d\sigma
\]

(2-16)

Eshagh et al. (2017) solved the integrations by assuming \( T = T_0 \) and obtained the compensation attraction of the gravity disturbance as follows:

\[
\delta g_C = G R \Delta \rho \int \frac{1}{r-n+1} \frac{T}{R} \left( 1 - \frac{n+2}{2R} \right) P_n(\cos \psi) d\sigma -

- G R \Delta \rho \int \frac{1}{r-n+1} \frac{T_0}{(n+3)} \left[ 1 - \kappa^{n+3} \right] P_n(\cos \psi) d\sigma
\]

(2-17)

Furthermore, they considered the spectral form of \( \delta g_C \) and got:

\[
\delta g_{C,n} = 4\pi G \Delta \rho \beta_n \frac{n+1}{2n+1} T_0 - 4\pi G R \Delta \rho \beta_n \left( 1 - \kappa^{n+1} \right) \delta_{n0}
\]

(2-18)

Where \( \beta_n = 1 - \frac{(n+2) T_0}{2R} \).
They proved by inserting Eq. (2-18) into (2-9) that the Moho depth can be obtained as:

\[ T = A_{c0} + \frac{1}{4\pi G\Delta\rho} \sum_{n=0}^{\infty} \frac{2n+1}{n+1} \tilde{\mu}_{n}^{-1} \left( \delta g_{n}^{\text{rb}} + \delta g_{n}^{\text{s}} + \delta g_{n}^{\text{cryst}} - \delta g_{n} \right) \]  

(2-19)

Where \( A_{c0} = \frac{R}{3} \left( 1 - \kappa^2 \right) \left( \frac{R}{R - T_0} \right) \). As it can be seen in Eq. (2-19), \( T_0 \), besides the zero-degree term, affects all frequencies.

3. The Iran case study

In this section, we present the Iran case study and the application of the three methods previously described to the gravimetric estimate of the Moho in Iran. We divide this section into four parts. In section 3.1 we present a brief geological structure of the area. The used gravity data are described in section 3.2 while in section 3.3 the local gravity Moho estimates over the study area by collocation, the Jeffrey and Sjöberg methods are presented. Finally, in section 3.4 comparisons among different gravimetric and seismic derived Moho values are shown.

3.1 The study area

All methodologies have been applied in Iran over an area limited by the parallels 20° and 45° North and the meridians 40° and 65° East (see Fig. 1). Several unique events like tectonics and orogenic activities led to complicated structural units in this area. By considering the geological features of Iran, some models and interpretations have been proposed for this region (Nabavi, 1976, Eftekharnenezhad, 1980, Alavi-Naini, 1993, Aghanabati, 2004, Ghorbani, 2013). According to these studies, a geological setting of this area showing a geological classification of various structural zones of Iran has been devised and is presented in Fig. 1, superimposed on the regional topography. Topography/bathymetric heights were generated by the SRTM30_PLUS model to degree and order 2160 with a resolution of 5′×5′ over the study area (Becker et al., 2009). As seen in Fig. 1, the ranges of topography vary from -3182 to 4142 m. Significant topography is seen over the Alborz and Zagros mountains which continues from West-North until East-South. Most of Iran is surrounded by a rough topography except for southern border of Caspian Sea, Central Iran, Lut Block, Jazmourian and Makran basins.
The convergence of the Arabia-Eurasia plate led to the complex features in the Iranian crust and lithospheric mantle. The closure of Tethys Ocean and collision of Arabian-Eurasian plates caused the formation of Iranian plateau during the Mesozoic and Cenozoic period (Berberian and King, 1981, Berberian et al., 1982). Some active and young tectonic structures consist of the collision zones in Zagros, Alborz, Kopeh-Dagh and subduction zones in the Makran and South Caspian Basin were formed as a result of the Arabia-Eurasia convergence (Shad Manaman et al., 2011). This convergence led to formation of the two tectonometamorphic and magmatic belts of Sanandaj-Sirjan zone and the Urumieh-Dokhtar magmatic assemblage.

Central Iran is a triangle located in the middle and bordered by the Alborz Mountains in the North, Lut Block in the East and Urumieh-Dokhtar in the South. In this zone, there are rocks of all ages, from Precambrian to Quaternary, and several episodes of orogeny, metamorphism and magmatism. Sanandaj-Sirjan is located to the South-West of Central Iran and the North-East of Zagros Mountains. A remarkable feature of this zone is the presence of immense volumes of magmatic and metamorphic rocks of Paleozoic and Mesozoic eras. Zagros ranges separate the Arabian Block from the rest of Eurasian tectonic plate. In this area, there are no abundant outcrops of Paleozoic rocks and the area is without magmatic and metamorphic events. Alborz range is located in North of Iran, parallel to the Southern margin of Caspian Sea. This mountain is characterized by different sedimentary rocks. The Kopeh-Dagh Mountains and basin consist largely of extrusive igneous rocks belong to Paleogene volcanic areas. Makran is separated from Jazmourian depression by a long range of ophiolites extending from West to East (cf. Ghorbani (2013)).
3.2 The gravity data set

In this study, the considered gravity data have been synthetized from the GOCO03S gravitational model up to degree and order 180 and were computed on a 0.5×0.5 arc-deg surface grid. In order to obtain the topography/bathymetry (TB) corrections, we applied the spherical harmonics expansion of digital elevation model from SRTM30_PLUS to degree and order 180 consistent with the resolution of CRUST1.0 model. Moreover, for computing the gravity corrections due to sediment and consolidated crustal layers, we used the Earth’s crustal model CRUST1.0, which in this area gives mean densities values for the sediments and the consolidated crustal layers that are, respectively, 2060 kg m$^{-3}$ and 2670 kg m$^{-3}$ (see Fig. 2b and 2c). By applying all these corrections we obtained the gravity data that were used in the inversion procedures. Fig. 2d represents the map of the refined Bouguer gravity, in unit of mGal, reduced for the gravitational contribution of crustal density heterogeneities over the
study area. This illustrates the largest and positive value at Oman Sea and the negative one over the Zagros and Sanandaj-Sirjan belts and in the North-East part of Iran around its border to Azerbaijan and Turkey and in the south part in Bam. All the mentioned corrections are displayed in Fig. 2 and the related statistics are given in Table. 1.

**Table. 1** Statistics of the TB, sediment and consolidated crust corrections to gravity disturbances [mGal]

|       | Max  | Mean | Min  | STD  |
|-------|------|------|------|------|
| TB    | 227.3| -35.0| -371.1| 96.7 |
| sediments | 183.5| 66.0 | 3.9  | 34.5 |
| crust | 46.5 | -199.5| -424.7| 84.2 |
| total | 486.8| 230.6| -195.1| 123.2|

![a) Image](image1.png) ![b) Image](image2.png) ![c) Image](image3.png) ![d) Image](image4.png)
Fig. 2 a) the TB gravitational effect; b) the gravitational effect of sediments; c) the gravitational effect of consolidated crust; d) the reduced Bouguer gravity anomalies [mGal].

3.3 The gravimetric Moho estimates

The three methods described in section 2 for determination of Moho were applied in the study area. The computations were accomplished by setting $T_0 = 44$ km, which is the mean of depths estimated from seismic studies (Mangino and Priestley, 1998, Paul et al., 2006, Taghizadeh-Farahmand et al., 2010, Radjaae et al., 2010, Tatar and Nasrabadi, 2013, Taghizadeh-Farahmand et al., 2015, Motaghi et al., 2015, Abdollahi et al., 2018).

As stated above, the collocation approach in planar approximation has been applied to GOCE derived reduced Bouguer gravity, i.e. Bouguer gravity anomalies reduced for sediment and consolidated crust effects. Moho depths have been determined with respect to mean value $T_0$ while the $\varepsilon$ values have been obtained according to the scheme described in section 2. In this computation, the constant density contrast between crust and mantle has been set to 600 kg m$^{-3}$. The gravity data, obtained by applying combined topography/bathymetry gravitational effect from SRTM30_PLUS data and corrections for the sediment and consolidated crust data generated from the CRUST1.0, has been re-gridded on a regular (x,y) grid in the investigation area (see Fig. 3):
The collocation procedure has been then applied iteratively. The behaviour of the empirical covariance function of gravity data and the best-fit model with the related parameters can be seen in Fig. 4 for the three steps that have been performed to get the final estimate.

a) First step: $\hat{A}_{dg} = 14000$ mGal$^2$, $\hat{\alpha} = 0.0055$ km$^{-1}$, $\sigma_n^2 = 815$ mGal$^2$
b) Second step: \( \hat{A}_{\delta g} = 3200 \text{ mGal}^2, \hat{\alpha} = 0.0135 \text{ km}^{-1}, \hat{\sigma}^2 = 290 \text{ mGal}^2 \)

c) Third step: \( \hat{A}_{\delta g} = 900 \text{ mGal}^2, \hat{\alpha} = 0.0317 \text{ km}^{-1}, \hat{\sigma}^2 = 192 \text{ mGal}^2 \)

**Fig. 4** The empirical covariance function of the gravity data and the best-fit model

In this figure, parameter \( A \) is the covariance value in the origin, \( \alpha \) is the scaling factor for argument of Bessel function and \( \hat{\sigma}^2 \) is the noise variance, i.e. the difference between the empirical value and the model function at the origin. \( A \) and \( \alpha \) are found by letting the first empirical zero coincide with the zero of the model function and assuming the model function coincide with the empirical one at the second point (Barzaghi et al., 1992). In the first step, the model function which best described the empirical values is \( J_1 \) Bessel function divided by its argument, with \( A=14000 \text{ mGal}^2 \) and parameter \( \hat{\alpha} =0.0055 \text{ km}^{-1} \). A value is sufficiently close to initial one of empirical function, which is 14815 mGal². The difference between the two values in the origin, i.e. the noise variance, has been fixed to 815 mGal². In the second step, residuals of gravity from the first inversion step have been used as input data. As can be
seen in Fig. 4 the variance of these residuals, i.e. the value in the origin of the empirical
function, decreased drastically to 3490 mGal$^2$ and the signal variance, i.e. the $A$ value, has
been set to 3200 mGal$^2$. The $\hat{\alpha}$ and $\hat{\sigma}_n^2$ quantities have been fixed at 0.0135 km$^{-1}$ and 290
mGal$^2$, respectively. Furthermore, in third step, based on the residual gravity from the second
iteration, model covariance parameters were fixed at $\hat{\alpha}_g = 900$ mGal$^2$, $\hat{\alpha} = 0.0317$ km$^{-1}$, $\hat{\sigma}_n^2 = 192$ mGal$^2$. This iterative process has been stopped at the third iteration since the covariance
function of the third step residuals has a correlation length (the distance at which the
covariance function is half of its value in the origin) that is comparable with the grid step.
Results of this procedure are shown in Fig. 5 and related statistics are summarized in Table 2.

![Maps](image)

**Fig. 5** Map of Moho model derived from collocation method in a) First step b) Second
The final estimate (see Fig. 5c), obtained by adding the $\Theta_i$ values coming from the iterative procedure to the mean depth $T_0 = 44$ km, shows maximum depths under the Zagros Mountain, the Sanandaj-Sirjan and the Urumieh-Dokhtar belts with spread under the Alborz Mountain and Kopeh-Dagh, while the minimum depth is under the Oman Sea and the border of Caspian. In first step it can be observed that the Moho depth varies between 35.5 km and 49.0 km and in most areas, depth of Moho is below 40 km. In second step, statistics are similar to previous with a slight increase of the standard deviation of the estimated Moho depths. As seen in Fig. 5c the Moho depths coming from the third step are more high frequency (standard deviation increases to 3.4 km) and ranges between 31.6 km and 54.6 km.

Based on gravity disturbance data, coming from the GOCO03S, completed to degree and order 180, we then estimated the Moho depth over Iran with the gravimetric approaches devised by Sjöberg and Jeffrey. As done in the collocation solution, the mean Moho depth has been set to 44 km. Also, the constant density contrast between crust and mantle has been set to 600 kg m$^{-3}$ and corrections including topography/bathymetry, sediment and consolidated crust has been accounted as well. The results are plotted in Fig. 6 and the summary of statistics is given in Table. 3. These solutions show a similar pattern with a large Moho depth under Zagros and Alborz mountains and also along Sanandaj-Sirjan and Urumieh-Dokhtar belts and Kopeh-Dagh. The areas with minimum depth are under the Oman Sea, some parts of Caspian and Persian Gulf while central Iran, Tabas and Lut block have relatively shallow Moho depth. As seen in Fig. 6, Sjöberg method gives a smoother solution than the one based on Jeffrey method.

Minimum Moho depths in both these methods are lower than minimum depths estimated using the collocation method. Statistics in Table. 3 show a minimum Moho depth of 17.6 km and 33.9 km for Jeffrey and Sjöberg methods, respectively. Also, the maximum Moho depth

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**Table. 2. Statistics of Moho depth computed according to the collocation method [km]**

| Collocation Method | Step   | Max  | Mean | Min  | STD  |
|--------------------|--------|------|------|------|------|
|                    | First step | 49.0 | 44.0 | 35.5 | 2.4  |
|                    | Second step | 51.9 | 44.0 | 32.8 | 3.0  |
|                    | Third step  | 54.6 | 44.0 | 31.6 | 3.4  |
according to Jeffrey solution seems to be overestimated since this method has given a depth around 67.4 km near the northwest of Iran. On the contrary, by applying the Sjöberg method, the maximum Moho depth in Iran has been estimated to 59.6 km.

Fig. 6 Map of Moho model derived from a) Jeffrey’s method b) Sjöberg’s method [km]

Table. 3. Statistics of Moho depth computed according to Jeffrey and Sjöberg’s method [km]

|       | Max  | Mean | Min  | STD |
|-------|------|------|------|-----|
| Jeffrey | 67.4 | 44.9 | 17.6 | 7.2 |
| Sjöberg | 59.6 | 46.6 | 33.9 | 3.7 |

3.4 Comparing gravimetric and seismic Moho estimates

To validate the gravimetric Moho solutions, we compared them with existing regional seismic studies for Iran (Mangino and Priestley, 1998, Paul et al., 2006, Taghizadeh-Farahmand et al., 2010, Radjaee et al., 2010, Tatar and Nasrabadi, 2013, Taghizadeh-Farahmand et al., 2015, Motaghi et al., 2015, Abdollahi et al., 2018). A compilation of these numerous seismic datasets has been prepared and checks for their consistency were performed. In this way, we defined a selected collection of seismic Moho values in the Iran area, which consists of 277 points. These models are shown in Fig. 7 and their statistics are given in Table 4. The maximum Moho depth is located under the Sanandaj-Sirjan zone and surrounding mountains.
By seismic estimates, the minimum depth of Moho is under the Oman Sea and Makran subduction zone. As it can be seen, Moho depths derived from seismic studies varies between 18.5 km and 66 km.

![Fig. 7 Moho derived from seismic results [km]](image)

| Statistics of Moho depth from Seismic estimates [km] |
|-----------|-----------|-----------|-----------|
| Seismic data | Max       | Mean      | Min       | STD       |
| Seismic data | 66.0      | 44.0      | 18.5      | 8.2       |

These seismic values were then compared with the gravity derived estimates. In order to perform the comparison, we interpolated the gridded gravity estimates on the sparse seismic point using linear interpolation.

The differences are plotted in Fig. 8 and the statistics of the differences are summarized in Table. 5. As one can see in Fig. 8a, the differences between the collocation solution and seismic data are between -17 km and 21.9 km. The differences between Jeffrey’s and Sjöberg’s solutions and seismic data range from -11.1 km to 22.2 km and -10.8 km to 23.4 km, respectively (see Fig. 8b and 8c).
Fig. 8 Differences between seismic data and Moho derived from a) Collocation method b) Jeffrey’s method c) Sjöberg’s method [km]

Table 5. Statistics of differences between gravimetric Moho estimates and seismic results [km]

| Method            | Max  | Mean | Min   | STD  | RMS  |
|-------------------|------|------|-------|------|------|
| Collocation Method| 21.9 | 2.4  | -17.0 | 6.3  | 6.7  |
| Jeffrey Method    | 22.2 | 5.7  | -11.1 | 6.1  | 8.3  |
| Sjöberg Method    | 23.4 | 5.2  | -10.8 | 6.0  | 7.9  |

As it can be seen in Table 5, the STDs of the differences with respect to seismic data are around 6 km, the smaller STD values being obtained by the Sjöberg estimate. Since the STD
of seismic data 8.2 km (see Table 4), we can conclude that the gravimetric Moho estimates are not so highly correlated with the seismic estimates. Furthermore, the statistics show that Jeffrey and Sjöberg’s method give estimated Moho values that have biases with respect to the seismic values larger than collocation. This reflects in the RMSs values that show how collocation gives a Moho estimate which is, overall, closer to the seismic values. This overall analysis can be further specified for different sub-areas in the Iran region where existing regional seismic solutions are available.

Central Zagros and specifically Sanandaj-Sirjan zone are regions where the maximum depth of Moho has been revealed therein. According to our computations, collocation solution indicated a 55 km Moho depth for this area. Sjöberg and Jeffrey’s methods also indicated Moho depths at the level of 55 km and 60 km for this zone, respectively. Dehghani and Makris (1984) by using integrated gravity and seismic data estimated a crustal thickness beneath the central Zagros in 55 km, which fully agrees with the results of collocation and Sjöberg’s methods. Hatzfeld et al. (2003) proposed a depth of 46 km for the crustal thickness at the single station close to the town of Ghir in central Zagros.

Another investigation of the lithospheric structure of the Iranian Plateau has been performed by Asudeh (1982) along three profiles connecting Mashhad to Shiraz, Tehran to Mashhad and Shiraz to Tabriz. He reported crustal thickness along these profiles 43, 45 and 46 km, respectively. Doloei and Roberts (2003) and Javan Doloei and Ghafori-Ashtiany (2004) have proposed 52 km for depth of Moho in Mashhad. By collocation solution, depth of Moho in Mashhad has been estimated in about 52 km which is in agreement with Javan Doloei (2003) and Javan Doloei and Ghafori-Ashtiany (2004) results. Also, Sjöberg and Jeffrey’s method estimated the Moho depth of about 52 and 56 km in Mashhad, respectively. Doloei and Roberts (2003) used seismic data and suggested a crustal thickness of 46 km in Tehran located southern part of the central Alborz. Results of collocation, Sjöberg and Jeffrey’s method gave values of Moho depths of 43, 45 and 47 km in Tehran, respectively.

Dehghani and Makris (1984) showed that the crustal thickness varies from 35 km beneath Alborz Mountains to 54 km in central Alborz. Sobouti and Arkani-Hamed (1996) identified a 45 km crustal thickness along the Alborz Mountains. In the analysis of 290 teleseismic events carried out by Sodoudi et al. (2009) at 12 short-period stations of the Tehran telemetric network, an average depth of 44-46 km for Moho under central Alborz has been estimated. Radjaee et al. (2010) reported the crustal thickness 48 km under the northern part of the central Iranian Plateau. Also, they found a variable crustal thickening between 55 and 58 km under central Alborz. Shad Manaman et al. (2011) estimated a thick Moho with 55-60 km
depth beneath the central Alborz. Jiménez-Munt et al. (2012) and Taghizadeh-Farahmand et al. (2015) estimated crustal thickness 50 and 54 km in central Alborz, respectively. The results of collocation and Sjöberg’s method indicated depth of Moho in that area around 53 km which is close to the values reported by Dehghani and Makris (1984), Radjaee et al. (2010) and Shad Manaman et al. (2011). The estimation of Jeffrey’s method has given a quite overestimated depth of 60 km in this area.

Paul et al. (2006) estimated crustal thickness beneath Urumieh-Dokhtar magmatic area around 42 km. Nasrabadi et al. (2008) indicated that Moho depth is 40 km beneath Maku station in northwest of Iran. Taghizadeh-Farahmand et al. (2010) applied P and S seismic waves to recover the crustal thickness around 48 km in this area. According to Taghizadeh-Farahmand et al. (2015), the average of Moho depth varies from 41 km in the northwest Iran to 45-49 km in the northeast. Jiménez-Munt et al. (2012) estimated the crustal structure from combination of the geoid height and elevation data with thermal analysis. Their results showed the crustal thickness of 50 km beneath the Alborz and Kopeh-Dagh mountains. By our gravimetric solutions depth of Moho in Kopeh-Dagh has been estimated slightly more than 50 km.

Mangino and Priestley (1998) estimated the Moho depth at 30-33 km beneath the South Caspian Basin. Also, Shad Manaman et al. (2011) estimated similar values for Moho depth in this area. Our results from gravimetric methods there indicate the Moho depth of about 37, 38 and 33 km by collocation, Sjöberg and Jeffrey’s methods, respectively.

Shad Manaman et al. (2011) investigated the Moho depth through the Makran subduction zone and reported values around 25-30 km for the Oman seafloor and Makran. Taghizadeh-Farahmand et al. (2015) presented a depth of 35 km over this area. Abdollahi et al. (2018) reported range of Moho from 18 to 28 km in Oman Sea. The collocation solution gave the Moho depth at around 33 km in Oman Sea. Also, results of Jeffrey and Sjöberg’s methods has led to depth values of 20 and 34 km in this area, respectively. Our estimations by collocation and Sjöberg’s method are different from the results of seismic studies at the subduction zone and the tectonic border in the Oman Sea. This could be related to the procedure that we adopted for correcting the gravity values. Indeed, Eshagh et al. (2017) concluded that the sediment and crystalline corrections computed using the CRUST1.0 have a low quality in oceanic areas.

Dehghani and Makris (1984) reported that the crustal thickness varies between 45 and 48 km in the eastern Iran. Nowrouzi et al. (2007) estimated depth of Moho around 44-50 km under Kopeh-Dagh. Jiménez-Munt et al. (2012) suggested Moho depth minima of about 36 km beneath the Lut block. According to Shad Manaman et al. (2011), Moho depth varies from 35
km to 40 km in central Iran and Lut block. Nasrabadi et al. (2008) mentioned that the crustal thickness deepens up to 56 km under the Naein station in central Iran. The results of Sadidkhoy et al. (2012) showed that depth of Moho in Isfahan area is variable between 38.5 and 43 km. Our solutions by gravimetric methods give the Moho depth ranging from 47 km in central Iran to 44 km in Lut block, which is in a good agreement with Paul et al. (2006) and Sadidkhoy et al. (2012). In the coast of the Persian Gulf, a Moho depth of about 25 km has been suggested by Paul et al. (2006) where we have different values (here our estimates are around 35 km). All these comparisons between seismic estimates and regional Moho depths obtained from the different gravimetric inversion methods for each of the different sub-areas have been summarized in Table. 6.

All in all, these comparisons show that our results are in most cases in the same range with seismic estimations in literature. By considering the effects of sediment and consolidated crust we provided satisfactory results for most of the continental crust where our estimates have a relatively good agreement with local seismic studies.

Larger discrepancies are present between seismic and gravimetric estimates in the offshore area around 22 degrees of latitude. This problem has to be further investigated also following the discussion presented in Eshagh et al. (2017).

Table. 6. The regional seismic Moho depths in sub-areas of Iran and differences with gravimetric solutions in this area [km]

| Region        | Reference                          | Moho Depth (km) | Differences between gravimetric solutions and regional seismic Moho depths |
|---------------|------------------------------------|-----------------|-------------------------------------------------------------------------|
| Central Zagros | Dehghani and Makris (1984)         | 55              | Collocation: 3.2  Jeffrey: 3.3  Sjöberg: 5.3 |STD  RMS  STD  RMS  STD  RMS |
|               | Hatzfeld et al. (2003)             | 46              |                                                                         |
|               | Motaghi et al. (2015)              | 49              |                                                                         |
|               | Tatar and Nasrabadi (2013)         | 47              |                                                                         |
| Central Alborz | Dehghani and Makris (1984)         | 35              | Collocation: 3.5  Jeffrey: 5.6  Sjöberg: 4.2 |STD  RMS  STD  RMS  STD  RMS |
|               | Sobouti and Arkani-Hamed (1996)    | 45              |                                                                         |
|               | Sodoudi et al. (2009)              | 44-46           |                                                                         |
|               | Radjae et al. (2010)               | 55-58           |                                                                         |
|               | Shad Manaman et al. (2011)         | 55-60           |                                                                         |
|               | Jiménez-Munt et al. (2012)         | 50              |                                                                         |
|               | Taghizadeh-Farahmand et al. (2015) | 54              |                                                                         |
| Region                          | Authors                      | Year(s)          | Values  | Values  | Values  | Values  | Values  |
|--------------------------------|------------------------------|------------------|---------|---------|---------|---------|---------|
| Northwest of Iran              | Nasrabadi et al. (2008)      | (2010)           | 40      | 48      | 4.8     | 5.0     | 4.7     | 9.9     | 4.3     | 5.9     |
|                               | Taghizadeh-Farahmand et al.  | (2015)           | 41      |         |         |         |         |         |         |         |
|                               | Dehghani and Makris (1984)   |                  | 45-48   |         |         |         |         |         |         |         |
|                               | Doloei and Roberts (2003)    |                  | 52      |         |         |         |         |         |         |         |
|                               | Javan Doloei and Ghafory-Ashtiany (2004) |                 | 52      |         |         |         |         |         |         |         |
|                               | Nowrouzi et al. (2007)       |                  | 44-50   |         |         |         |         |         |         |         |
|                               | Jiménez-Munt et al. (2012)   |                  | 50      |         |         |         |         |         |         |         |
|                               | Taghizadeh-Farahmand et al.  | (2015)           | 45-49   |         |         |         |         |         |         |         |
| Northeast of Iran              | Shad Manaman et al. (2011)   |                  | 40      |         | 3.0     | 7.4     | 5.5     | 13.0    | 3.5     | 11.2    |
|                               | Jiménez-Munt et al. (2012)   |                  | 36      |         |         |         |         |         |         |         |
|                               | Taghizadeh-Farahmand et al.  | (2015)           | 41      |         |         |         |         |         |         |         |
|                               | Nasrabadi et al. (2008)      |                  | 56      |         | 2.3     | 8.1     | 4.3     | 11.8    | 2.2     | 10.8    |
|                               | Motaghi et al. (2015)        |                  | 38      |         |         |         |         |         |         |         |
|                               | Taghizadeh-Farahmand et al.  | (2015)           | 42      |         |         |         |         |         |         |         |
|                               | Paul et al. (2006)           |                  | 41      |         | 1.1     | 5.3     | 1.2     | 8.2     | 0.5     | 6.4     |
|                               | Shad Manaman et al. (2011)   |                  | 35      |         |         |         |         |         |         |         |
|                               | Sadidkhouy et al. (2012)     |                  | 38.5-43 |         |         |         |         |         |         |         |
| Central Iran                  | Mangino and Priestley (1998) |                  | 30-33   |         | 10.5    | 7.6     | 10.4    | 7.6     | 13.9    | 10.9    |
|                               | Shad Manaman et al. (2011)   |                  | 30-33   |         |         |         |         |         |         |         |
| South Caspian Basin           | Paul et al. (2006)           |                  | 48      |         | 6.0     | 6.1     | 6.1     | 6.8     | 6.3     | 6.5     |
|                               | Motaghi et al. (2015)        |                  | 59      |         |         |         |         |         |         |         |
|                               | Taghizadeh-Farahmand et al.  | (2015)           | 48      |         |         |         |         |         |         |         |
| Urumieh-Dokhtar and Sanandaj-Sirjan | Paul et al. (2006)           |                  | 25-30   |         | 5.0     | 8.2     | 6.0     | 9.5     | 4.8     | 9.9     |
|                               | Motaghi et al. (2015)        |                  | 35      |         |         |         |         |         |         |         |
|                               | Taghizadeh-Farahmand et al.  | (2015)           | 48      |         |         |         |         |         |         |         |
|                               | Abdollahi et al. (2018)      |                  | 18-28   |         |         |         |         |         |         |         |
| Oman Sea Floor and Makran     | Shad Manaman et al. (2011)   |                  | 25-30   |         |         |         |         |         |         |         |
|                               | Taghizadeh-Farahmand et al.  | (2015)           | 35      |         |         |         |         |         |         |         |
|                               | Abdollahi et al. (2018)      |                  | 18-28   |         |         |         |         |         |         |         |
| Coast of the Persian Gulf     | Paul et al. (2006)           |                  | 25      |         | 1.6     | 3.2     | 2.6     | 8.1     | 3.9     | 5.0     |
4. Summary and concluding remarks

In this study, we applied collocation method as well as two approaches based on isostasy principle presented by Sjöberg and Jeffrey for estimating the regional Moho in Iran using gravity observations. For this purpose, we considered the data of the GOCO03S satellite only global geopotential model that were subsequently reduced by topography/bathymetry, sediment and crystalline crust data effect by using the SRTM30_PLUS DTM and the CRUST1.0 model. The three different gravimetric approaches gave coherent estimates. The estimated Moho depths obtained using collocation, Jeffrey and Sjöberg’s approaches proved to be statistically equivalent when compared to seismic derived values. The collocation method has been applied iteratively in three steps and the numerical computations showed that an iterative process in collocation method could not change the results significantly even though the Moho estimate based on collocation method in the third step contains more high frequency details. Furthermore, the collocation solution proved to be less biased than those based on Jeffrey and Sjöberg’s methods when considering discrepancies with respect to seismic Moho estimates. To evaluate our results, we have compiled a 277 points collection of local seismic estimations in this area. The overall standard deviation of the differences between the results of the collocation, Sjöberg and Jeffrey’s methods and the seismic estimates is around 6.0 km.

The minimum RMS of differences is between collocation estimates and point-wise seismic data since, as mentioned, collocation led to less biased discrepancies with the considered seismic values.

Although the application of sediment and consolidated crust corrections in our solutions provides a reasonable agreement with point-wise seismic data over most of continental areas like central Zagros, Sanandaj-Sirjan, Kopeh-Dagh and Alborz Mountains, this leads to unrealistic estimates under the Makran subduction zone, Oman Sea, Persian Gulf and Caspian Sea. This can be the effect of the poor quality of the CRUST1.0 data in this region (see Eshagh et al. (2017) ).

The comparisons performed in this paper prove that further analyses are needed to come to a better consistency between gravity and seismic derived Moho depths in Iran before computing any joint seismic/gravimetric estimate.
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