Spatially resolved spectroscopy across stellar surfaces

III. Photospheric Fe \textsc{i} lines across HD 189733A (K1 V)

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ABSTRACT

Context. Spectroscopy across spatially resolved stellar surfaces reveals spectral line profiles free from rotational broadening, whose gradual changes from disk center toward the stellar limb reflect an atmospheric fine structure that is possible to model by 3D hydrodynamics.

Aims. Previous studies of photospheric spectral lines across stellar disks exist for the Sun and HD 209458 (G0 V) and are now extended to the planet-hosting HD 189733A to sample a cooler K-type star and explore the future potential of the method.

Methods. During exoplanet transit, stellar surface portions successively become hidden and differential spectroscopy between various transit phases uncovers spectra of small surface segments temporarily hidden behind the planet. The method was elaborated in Paper I, in which observable signatures were predicted quantitatively from hydrodynamic simulations.

Results. From observations of HD 189733A with the ESO HARPS spectrometer at \( \lambda/\Delta \lambda \approx 115,000 \), profiles for stronger and weaker Fe \textsc{i} lines are retrieved at several center-to-limb positions, reaching adequate S/N after averaging over numerous similar lines.

Conclusions. Retrieved line profile widths and depths are compared to synthetic ones from models with parameters bracketing those of the target star and are found to be consistent with 3D simulations. Center-to-limb changes strongly depend on the surface granulation structure and much greater line-width variation is predicted in hotter F-type stars with vigorous granulation than in cooler K-types. Such parameters, obtained from fits to full line profiles, are realistic to retrieve for brighter planet-hosting stars, while their hydrodynamic modeling offers previously unexplored diagnostics for stellar atmospheric fine structure and 3D line formation. Precise modeling may be required in searches for Earth-analog exoplanets around K-type stars, whose more tranquil surface granulation and lower ensuing microvariability may enable such detections.

Key words. stars: atmospheres – stars: solar-type – techniques: spectroscopic – stars: individual: HD 189733A – line: profiles

1. Introduction

Three-dimensional and time-dependent hydrodynamic simulations provide realistic descriptions for the photospheres of the various classes of stars. The combination of stellar spectra computed from such models, with corresponding models of planetary atmospheres, constrain the properties of both the star and its exoplanets. To test and evolve such models, more detailed observations than the ordinary spectrum of integrated starlight are desirable. Spectral line syntheses from 3D atmospheres display numerous features in the gradual changes of photospheric line profile strengths, shapes, asymmetries, and wavelength shifts from the stellar disk center toward the stellar limb. Direct comparisons between theory and spectral-line observations were in the past carried out only for the spatially resolved Sun (e.g., Lind et al. 2017). This project extends such studies to other stars as well. In Paper I (Dravins et al. 2017a), theoretically predicted spatially resolved signatures were examined for a group of main-sequence stellar models with temperatures between 3960 and 6730 K. Corresponding observations are feasible during exoplanet transits when small stellar surface portions successively become hidden, and differential spectroscopy between different transit phases provide spectra of small surface segments temporarily hidden behind the planet. The observational requirements were elaborated in Paper I, in which observable signatures were predicted quantitatively. In Paper II (Dravins et al. 2017b), a first observational demonstration of this method was presented for the G0 V star HD 209458.

This Paper III extends such studies to another bright planet-hosting star but of lower temperature, the \( m_V = 7.7 \), K1 V star HD 189733A, circled by its planet HD 189733Ab. To avoid constantly repeating their (easily intermixed) numbers from the Henry Draper catalog, for the purposes of this paper we refer to HD 189733A as “Alopex”\textsuperscript{1}, and to HD 189733Ab as simply “the planet”.

Besides probing a cooler stellar atmosphere, there is a significance for exoplanet searches since the surfaces of K-type stars are predicted to be quieter, with lesser amplitudes in velocity and temperature than in hotter and more solar-like stars.

Searches for exoplanets that mimic the Earth in terms of mass and orbit are limited by intrinsic stellar microvariability in either apparent radial velocity or photometric brightness (Fischer et al. 2016), and therefore may appear less challenging around K-type stars. This requires adequate modeling of their surface convection so that, for example, correlations between

\textsuperscript{1} This name – Greek Λόφεξ – is taken from the original taxonomic name for the arctic fox (Alopex Lagopus) given by Linnaeus in 1758, here relating to the namesake of its constellation Vulpecula (Latin for ‘little fox’). It is also the Greek name for that constellation.
stellar fluctuations in brightness, color, and radial velocity are adequately understood and may be compensated for. However, given the often greater magnetic activity and increased spottness on such stars, separate treatments of magnetically sensitive features over the timescales of their variability may also be needed to disentangle exoplanet signatures.

Further, analyses of exoplanet atmospheres by transmitted starlight require the background stellar spectrum to be precisely known. That is not the averaged spectrum of the entire stellar disk but that from only the small area temporarily behind the planet, such that the varying stellar spectrum along the chord of transit has to be known for any more precise studies (Rackham et al. 2018).

Besides applying this method to a new target star, the aim is to explore its general practicality. Currently, large transiting planets with bright host stars are actively being sought by several photometric surveys. Recent and forthcoming high-resolution spectrometers at major telescopes are likely to observe such systems for exoplanet research; using this method, the same data can be used to probe also the host star.

2. Hydrodynamic atmospheres and their spectra

2.1. Three-dimensional structures on different stars

Three-dimensional and time-variable model photospheres are now established as realistic descriptions of stellar outer layers. Originating from initial modeling of the solar photosphere (e.g., Nordlund et al. 2009), simulations have now been extended to stars with widely different parameters over much of the Hertzsprung–Russel diagram (Magic et al. 2013; Tremblay et al. 2013). Although the basic physical processes are similar in giants, dwarfs, and even white dwarfs, synthetic surface images reveal the greatly changing granulation sizes on stars with different surface gravity, as well as how the granulation brightness contrast increases with temperature, at least for stars comparable to the Sun. In disk-integrated starlight, predicted observable quantities include photometric microvariability and flickering (Samadi et al. 2013a,b). Signatures of the surface granulation might also be observable during exoplanet transits as an additional intensity fluctuation (with a certain correlation between different colors) caused by its temporal variability on spatial scales that are differently sampled by planets of dissimilar size (Chiavassa et al. 2017). Other classes of predictions differing between classical 1D and 3D models are those of stellar limb darkening (Magic et al. 2015) and of photometric colors (Kučinskas et al. 2018).

Of particular relevance for cool K-type stars such as Alopex, is that the granulation contrast is predicted to be rather lower than in somewhat hotter stars more similar to the Sun. Not only does the amplitude of convection itself get reduced, but also the extent to which its effects are visible on the stellar surface. The lower effective temperature of course implies a lower stellar flux but also decreases the atmospheric opacity at a given pressure, correspondingly increasing the characteristic densities near the surface. Thus, the stellar surface (optical density \( \tau \sim 1 \)) is located at higher densities. With higher densities and less convective flux, smaller velocity and temperature amplitudes suffice to transport the stellar flux outward. Further, the opacity structure enables radiative diffusion to carry a substantial fraction of the flux in the layers just below the visible surface, reducing the convective flux in the visible layers to only a small fraction of the total. For modeling details and comparisons between synthetic granulation images for stars at different temperature, see Magic et al. (2013), Nordlund & Dravins (1990), and Tremblay et al. (2013).

2.2. K-dwarf surface spectroscopy

As stressed in Paper I, the simulation of 3D atmospheric hydrodynamics is only a first part of the problem since most astrophysical deductions about stellar or planetary properties require synthetic spectra for comparison; see, for example, Asplund et al. (2000), Asplund (2005) and Chiavassa et al. (2018). Synthetic spectral lines from such K-type stellar models have been computed by Dravins & Nordlund (1990b) and Ramirez et al. (2009). The lower amplitudes of convective motion and lesser temperature contrast result in smaller convective wavelength blueshifts and weaker curvatures of stellar bisectors, as compared to, for instance, the solar case. Some observations have been made to seek evidence of the surface structure on Alopex and other K-type dwarfs. Thus, Ramirez et al. (2008) obtained high-resolution spectra of several K-type dwarfs to identify asymmetries in differently strong Fe I line profiles that have C-shaped bisectors as signatures of granulation.

Specifically for Alopex, observational confrontations with 3D models have been carried out in analyzing photometric light curves during transit, searching for effects to segregate between limb-darkening functions predicted from 1D and 3D model atmospheres. The differences are small, however, and largely masked by the great amount of absorption lines, whose different and complex center-to-limb behavior largely masks the underlying temperature structure (Hayek et al. 2012). If extremely good photometric precision could be achieved, polarimetric observations during transit could offer further constraints on atmospheric structure, as simulated by Kostogryz et al. (2017).

An ambitious study to deduce the center-to-limb variation of the strong absorption lines of Ca II H & K and Na I D1 & D2 lines was carried out by Czesla et al. (2015), recording transit spectra of Alopex with the ESO UVES spectrometer. The wings of these lines were found to be limb-brightened relative to the spectral continuum, in agreement with models. Understanding the behavior of such very strong lines is essential for exoplanet atmospheric studies, since these are the types of lines in which their atmospheres can be detected. However, corresponding behavior at line centers could not be identified because this behavior was masked by variable stellar activity.

3. HD 189733A (Alopex): The star and its planet

Although the principle of differential spectroscopy during exoplanet transit may appear to be relatively straightforward, its practical implementation requires observations at very high signal-to-noise (S/N), as emphasized in Paper I. Transiting planets cover only a tiny fraction of the stellar surface, which currently limits the method to the brightest planet-hosting stars with the largest planets. In this work, this method is applied to HD 189733A (Alopex). Its transiting planet covers ~2.5% of the stellar surface and produces the deepest transit among the currently known brighter host stars (Fig. 1 in Paper II). We used photometry from the Hubble Space Telescope (HST) by Pont et al. (2007), who measured the transit depth as 2.6% of the stellar irradiance (Fig. 1). The precise value, however, depends on the exact wavelength range, and its limb darkening at the chord of transit.
Along with its apparent brightness and deep photometric transit, an advantage in choosing this target is that its planet HD 189733AB has, since its discovery (Bouchy et al. 2005), been intensely studied, and many data are available in various archives. The system remains a prime target for exoplanet atmospheric studies and is certain to be observed with future instrumentation.

Numerous studies of the planet, including the dynamics of its extended atmosphere, have been made. Daytime temperatures of ~1200 K in line-forming regions (e.g., Knutson et al. 2007; Line et al. 2016) imply a bloated atmosphere with layers of light gases and molecular constituents such as H₂O, CH₄, and CO₂. While this inflated state enables the study of the planet's atmosphere and mass loss, the presence of spectral lines from such planetary species along with the different effective planet sizes in the corresponding monochromatic light imply that constructions of the observed (star+planet) spectra at the precise wavelengths corresponding to such molecular lines could be a more complex task; we do not attempt this approach in this work. Rather, this study targets stellar photospheric Fe lines, whose formation requires temperatures much higher than the planetary temperatures, and where the optical density of the planetary atmosphere (and thus the effective planet size) is not expected to change across such lines. At such wavelengths, it must be a closely valid approximation to treat the planet as an opaque body, whose size is indicated by transit photometry in adjacent passbands.

3.1. Stellar properties

The Alopex effective temperature is close to that of the well-studied K-giant Arcturus and their spectra are rather similar. This resemblance to the extensively charted spectrum of Arcturus greatly facilitates the identification of spectral lines in Alopex, further eased by its low rotational velocity (Cegla et al. 2016; Strachan & Anglada-Escudé 2017; Torres et al. 2012), which produces relatively unblended lines despite a dense spectrum. Overall stellar parameters have been deduced and compiled by numerous authors. By combining interferometric observations of the limb-darkened angular diameter with several other measurements, Boyajian et al. (2015) deduced $T_{\text{eff}} = 4875 \pm 43$ K, a stellar linear radius $R_\star = 0.805 \pm 0.016 R_\odot$, and $\log g [\text{cgs}] = 4.56 \pm 0.03$. The metallicity is given by Torres et al. (2008) as $[\text{Fe/H}] = -0.03 \pm 0.08$.

For the identification of many hundreds of spectral lines in Alopex, spectrum atlases of Arcturus are used as a guidance. We recall the main parameters for that giant star as $T_{\text{eff}} = 4286 \pm 30$ K and $\log g [\text{cgs}] = 1.66 \pm 0.05$ (Ramírez & Allende Prieto 2011). Although this, of course, is a very different object, its temperature and spectrum are sufficiently close to those of Alopex, as to often enable straightforward line identifications, analogous to how lines in the G0 V star HD 209458 could be identified in Paper II using solar spectrum atlases.

3.2. M-dwarf companion

Alopex is the primary of a double star system, accompanied by a mid-M dwarf, HD 189733B, with a separation of 11.2 arcsec on the sky, corresponding to a projected distance of ~216 au (Bakos et al. 2006). Astrometric measurements suggest that the orbit of the secondary lies nearly in the plane of the sky (i.e., perpendicular to the orbital plane of the transiting planet) and has a period of ~3200 yr. Such a wide binary does not perceptibly influence the surface structure of Alopex; also practically no spectrometer straylight is expected from this well-separated and faint companion, and there is no measurable change in stellar radial velocity during the hours of a planetary transit.

3.3. Stellar activity

Alopex is photometrically variable (classified as a BY Dra type star) that has an active chromosphere (Boisse et al. 2009; Strassmeier et al. 2000; Winn et al. 2007) and a magnetic field (Fares et al. 2010). Long-term photometric monitoring shows somewhat erratic variations following a quasi-periodic cycle of around 12 days, with an amplitude of ~3% at visible wavelengths. This is obviously the period of stellar rotation (Henry & Winn 2008) and the amplitude of such light variations is equivalent to a Jupiter-sized dark spot with temperature ~1000 K cooler than the photosphere, rotating into and out of view. The variability also manifests itself as a jitter in the apparent radial velocity on a level of ~10 m s⁻¹ (Lanza et al. 2011; Winn et al. 2006). From space photometry, there is no evidence for any additional transiting planets, moons, or rings (Croll et al. 2007; Pont et al. 2007).

The presence of stellar activity offers both opportunities and problems. Precision photometry during transit suggests that the planet sometimes crosses some dark spots (Pont et al. 2007; Sing et al. 2011), while bright flares may appear in chromospheric emission lines (Czesla et al. 2015; Klocová et al. 2017). A challenging future task will be to recover spatially resolved spectra of such starspots and active regions (including their magnetic signatures), but that will require simultaneous sequences of precision photometry and spectroscopy, which are not yet available. For the present project, it introduces a slight uncertainty from using an average transit light curve, while the spectra originate from different transits. Some recordings could possibly be from instances when the planet happened to cross some starspot, and the error budget for the retrieved spectra would then be enhanced by an unknown ratio of contributions from the magnetic and quiet photospheres. However, Alopex is not strongly variable (especially not on short timescales comparable to the transit times) and its starspot area coverage is small, likely adding only a minor contribution to the error budget. As seen in photometric light curves spanning several 12-day rotation periods (Strassmeier et al. 2000), the variability almost entirely follows the rotation period and has only small fluctuations on shorter timescales. However, without simultaneous photometry, any recovery of spatially resolved chromospheric emission lines would be uncertain and will not be attempted here.

4. Planet HD 189733Ab

The planet has been extensively studied with numerous instruments (not least in the infrared) for emission and transmission spectroscopy, inferring its atmospheric day-night thermal structure, a planetary hotspot near the substellar point, atmospheric winds, dust, molecules and atoms in the evaporating upper atmosphere, etc. For this project, however, our main interest lies in the geometric size of the planet at those visual wavelengths at which our spectroscopic analysis is to be carried out, as well as knowing the transit path along the chord across the star. Being slightly larger than Jupiter, the apparent radius of the planet was deduced from observations with the ACS instrument on the HST as 0.1572 ± 0.0004 $R_\oplus$ (Pont et al. 2007), while various wavelength passbands in the HST STIS instrument yielded values between 0.15617 and 0.15754 $R_\oplus$ (Sing et al. 2011). Ground-based data show only very slight variation among various wavelength bands.
in the optical (Borsa et al. 2016). Even in the far-infrared, the relative area covered by the planet (the square of these numbers, 2.46%) remains about the same (Agol et al. 2010; Beaulieu et al. 2008). For our later calculations, this implies that choosing the exact wavelength band for the photometric transit should not be critical.

4.1. Planetary orbit and transit geometry

The geometry of the planetary transit must be known to fully interpret any observed line-profile variations. Through the Rossiter–McLaughlin effect, the position and path of the planet across the stellar disk can be determined. Details of that method are explained in, for example, Gaudi & Winn (2007) and Hirano et al. (2010, 2011). Different authors deduce slightly different values for the various parameters but in a critical review of compiled data, Torres et al. (2008) confirmed that the planet moves in an almost circular prograde orbit of period $2.21857312 \pm 0.00000076$ days and has an inclination of $85.58 \pm 0.06^\circ$. That value is measured relative to the plane of the sky such that a value of $90^\circ$ implies a transit through the center of the stellar disk. The orbital radius of $8.863 \pm 0.020 R_\star$ gives an impact parameter (minimum sky-projected distance to stellar disk center, in units of $R_\star$) of $b = 0.6631 \pm 0.0023$ (Agol et al. 2010). The planet reaches its point closest to stellar disk center at $\mu = \cos \theta = 0.75$, where $\theta$ is the angle between the vertical from the stellar surface and the direction toward the observer. It is somewhat more difficult to determine the inclination of the stellar rotation axis to the plane of the sky. Henry & Winn (2008) found a lower limit of $54^\circ$, which is consistent with the stellar spin being aligned with the planetary orbit. More recent discussions of specific stellar parameters are by Cegla et al. (2016), Collier Cameron et al. (2010) and Triaud et al. (2009).

4.2. Photometric transit

The time of each mid-transit is obtained from the ephemeris as $T_j = T_0 + jP$, where $T_0 = 2453988.80336$ MJD is a reference transit transit time, $P = 2.21857312$ d is the orbital period of the planet (Extrasolar Planet Encyclopedia 2017), and $j = 1, 2, 3, \ldots$ the sequential transit event. The maximum photometric transit depth reached during the 109.6-min. transit is 2.6% in the visible. With the impact parameter $b = 0.663$, the transit occurs at stellar apparent latitude $34^\circ$ and the length of the transit path equals 0.749 stellar diameters. With the planet diameter $0.157 \times$ stellar, the transit proceeds with one planet diameter per $\sim 23$ min, and thus exposes much shorter than that do not result in significant spatial smearing (except perhaps very close to the limb).

To retrieve the spectrum temporarily hidden behind the planet at each transit epoch, the fraction of the flux then removed by the planet must be known. This fraction of hidden flux, or effective planetary area, $A_{\text{eff}}$ (in units of full-disk stellar flux), is the product of the local stellar brightness and the area of the planet. Since the transits are repetitive, it is possible to use such data from different transit events from those of the spectroscopic measurements. We obtained the values of $A_{\text{eff}}$ from the photometric light curve measured by Pont et al. (2007) with the ACS instrument on the HST (Fig. 1). Of course, this value could also be calculated from the transit geometry and limb-darkening law of the star; however our procedure is model independent and does not assume any stellar limb-darkening model. As remarked above, because of its atmosphere, the effective size of the planet may slightly vary with wavelength. However, the photometric transit observations with the HST ACS cover 550–1050 nm, largely overlapping our spectral region. Actually, the measured transit light curves differ only slightly between different optical passbands, and reconstructed line profiles were found in Paper II to be not sensitive to modest errors in effective planetary area.

4.3. Barycentric motion and astrocentric correction

The measured velocity semi-amplitude induced on the host star by the planet over its orbital period is $K = 205 \pm 6$ m s$^{-1}$ (Bouchy et al. 2005). Since the eccentricity is close to zero (Boisse et al. 2009), i.e., the orbit is nearly circular, the barycentric radial-velocity motion of the star can be closely approximated by a sinusoid with amplitude 205 m s$^{-1}$. Such a function was adjusted to extract the heliocentric velocities to astrocentric values, thus placing the stellar spectra on a static frame-of-reference relative to the stellar center of mass.

5. Spectroscopic data

As detailed in Papers I and II, the S/N requirements limit usable data to the highest fidelity spectra from high-resolution spectrometers. For example, if one desires a signal to noise in the reconstructed spectrum on the order of 100, say, extracted from only $\sim 2\%$ of the total stellar signal, this requires an original
S/N around 5,000. This is compounded by the center-to-limb decrease of stellar surface brightness. While its amount depends on the wavelength region, it is more pronounced for cooler stars, there also enhanced by absorption-line contributions. The limb darkening for Alopex was studied by Hayek et al. (2012), who found that the surface brightness in the $U$, $V$, and $I$ photometric bands decreased to 70, 80, and 87% of their disk-center values at half a stellar radius from disk center, and to 35, 50, and 66% at 0.9 radii, making near-limb measurements particularly challenging. The observed signal was shown in Fig. 1 while modeled continuum values for other stellar models are in Fig. 12.

Fortunately, Alopex is among the objects of which extensive observations have been carried out and numerous spectra are available in observatory archives. For the study of stellar photospheres, spectra in the visual region are preferred: in the ultraviolet there is too much stellar line blending and in the infrared the paucity of stellar lines is compounded by telluric absorption bands.

After searching the archives of several major observatories, suitable data sets covering the planetary transit were identified from the ESO UVES and HARPS spectrometers. From these, two observing runs with HARPS (High Accuracy Radial velocity Planet Searcher) were selected. Having two independent data sets enables both the combination of their data, and also the ability to check the results from one against the other. The HARPS instrument is a high-resolution ($\Delta \lambda/\Delta \lambda \approx 115,000$) spectrometer with an excellent wavelength stability on the order of 1 m s$^{-1}$ (Mayor et al. 2003). Light from the ESO 3.6 m telescope is fiber-fed to an echelle spectrometer covering 380–690 nm over 72 echelle orders, recorded onto two CCD detectors. The data selected originate from two observing runs on July 19 and August 28, 2007, respectively. Each of these contain sequences of 20 exposures during the actual transit, each with 300 s exposure time, as well as a similar number of exposures outside transit. During the hours of transit, as observed through airmasses around 1.7, photometric S/Ns (as computed by the data reduction pipeline for the better-exposed echelle orders) were drifting around 100–120 per spectral resolution element. For more details, see Gustavsson (2017).

6. Data analysis

Extracting a stellar spectrum from the small area covered by a transiting planet requires a S/N much higher than available in individual spectral exposures. Since photospheric lines that share similar parameters are formed in a similar manner within the stellar atmosphere, numerous such lines may be averaged to obtain a low-noise representative profile. Similar to Paper II, we selected Fe I lines since these are numerous and have been studied and modeled in many other contexts. A difference from the G0V star HD 209458 in Paper I, however, is the significantly more crowded spectrum of the cooler Alopex, which offers more numerous lines but also poses some challenges for the precise line extraction.

6.1. Identifying spectral lines

The temperature of the K1-dwarf Alopex is not much different from that of the K0-giant Arcturus, one of the few stars with extensive line identifications in a high-resolution spectral atlas (Hinkle et al. 2000). Further, the metallicity of Alopex is not substantially different from that of the Sun, and they have many spectral lines in common. Hundreds of lines need to be selected to reach the required S/N, and for their selection, we started with a listing of apparently unblended solar lines, verified their presence in the spectrum of Alopex, and also checked the identified lines against the Arcturus spectrum to remove those that can be suspected to be blended or contaminated by others. Having a clear empirical footing, we prefer this procedure to, for example, using a synthetic spectrum from an atomic-line database run through a stellar atmosphere model.

6.2. Selecting Fe I lines

We started with the list of 402 largely unblended solar Fe I lines by Stenflo & Lindegren (1977) to identify prospective lines. Out of these, 373 could be identified in the spectrum of Alopex, while slightly less than half (158) were found to be reasonably unblended. Their distribution is shown in Fig. 2, plotted as observed absorption down from the continuum. Detailed line data are given in Tables A.1 and A.2.

6.3. Continuum determination

While the HARPS data do have exquisite wavelength stability, the photometric retrieval of continuum-normalized line profiles is somewhat complex because of the rapidly varying intensities in the dense spectrum where often no true stellar continuum is reached next to the line, which is why a wider interval has to be examined. To limit the effort, a standardized procedure was applied. After locating a spectral interval of ±0.15 nm around any candidate spectral line, we found a first-order estimate of the local continuum by first normalizing to the largest local intensity value and then dividing by the median of flux values above 95% in intensity. For these selections, regions close to the strongest lines were avoided. To find the central wavelength of a line (in order to enable its later placement for averaging on a common velocity scale), we carried out a nonlinear least squares fit with a five-parameter Gaussian function to the immediate vicinity of the line (covering ±0.04 nm), from which values for the local continuum and of the line center position were obtained. This is of the type $I + (\lambda - \lambda_0) \Delta I/\Delta \lambda - I_0 \cdot \exp[-((\lambda - \lambda_0)/w)^2]$, where $I$ is the continuum level, $\Delta I/\Delta \lambda$ the slope of the continuum, $\lambda_0$ the nominal wavelength from the line list, $I_0$ the line-center intensity, $\lambda_0$ the line-center wavelength, and $w$ the line width. Using these
values, we next transformed the wavelength scales to equivalent Doppler velocities, applying the astrocentric wavelength correction as above, and placing all lines on a common intensity and wavelength scale. Figure 3 shows a sample of the superposition of profiles of a few Fe i lines from many successive exposures, illustrating typical levels of reproducibility and noise.

6.4. Line averages and reference profiles

The group of 158 selected lines was subdivided into two for strong and weak lines, respectively, splitting the groups at observed central absorption depths below or above 55% of the apparent continuum. By forming their averages (over 72 and 86 lines for the strong and weak groups, respectively), representative low-noise profiles for lines of different strength were obtained. Figures 2 and 4 show this line selection and their averaging. For the strong-line group, the average wavelength is 558.3 nm, average line-depth intensity equals 40.9% of the continuum, and average excitation potential \( \chi = 3.26 \text{ eV} \). For the weak-line group, the averages are 581.6 nm, 73.6%, and 3.77 eV. The respective standard deviations in the wavelength distribution for the strong- and weak-line groups are 65 and 66 nm, and 1.07 and 0.89 eV for the excitation potentials (Tables A.1. and A.2.). We note that these are the observed line strengths, in which the intrinsic stellar spectrum has been degraded by the finite spectrometer resolution.

The averaging of line profiles is carried out in velocity space, individually scaling each observed line profile. After finding the position of any line center, relative wavelength positions are converted to equivalent Doppler velocities, and the intensities linearly averaged. We note that this would be equivalent to averaging in Fourier space as applied by, for example, Gray (2016), only with possible slight differences in how noise properties are propagated.

Experiments were also made with various subsets of these lines, all of which must of course be blended to at least some small extent. For example, the same analysis as above was carried out by retaining only smaller subsets of more strictly unblended lines. If required to be surrounded by an apparent continuum of at least 95% intensity over \( \pm 15 \text{ km s}^{-1} \), 74 out of these 158 lines remained. However, in the end, no significant difference in results was seen, suggesting that the weak blends present seem to be of random character and do not contribute systematic effects.

The averages of lines in Fig. 4, with each individual profile starting with \( S/N \geq 100 \), begin to approach S/Ns on the order of 1,000 for each exposure (i.e., for the stochastic part of the noise). However, this is still not adequate and additional averaging is needed to further enhance the signal. Half of the about 80 exposures from the two observing runs are recorded outside transit, and these are next averaged to produce a low-noise reference spectrum against which the spectra recorded during transit are to be contrasted.

By first forming such an average over all \( 20 + 19 = 39 \) exposures recorded outside the two transits, and then over the many lines in each line group, averaging is achieved over \( \sim 2,500 \) profiles and the nominal S/N can be expected to reach \( \sim 5,000 \). Equally low-noise spectra cannot be obtained for each transit phase, however. With 20 in-transit exposures for each of the two observing runs, a total of 40 exposures are available over the transit chord. To push the S/N, we divide the transit chord into 10 epochs and, for each of these, collate two exposures from each observing run to obtain the average of four exposures from each transit epoch; this increases the critical S/N by a factor two at the cost of somewhat decreasing the spatial resolution.

6.5. Line profile ratios during transit

The change in the spectrum during the various transit epochs relative to the full-disk spectrum outside transit is tiny and not easily discernible in an ordinary line-profile format. Figure 5 instead shows the ratios of line profile intensities at each different transit epoch relative to the reference profile from outside transit (for clarity, only every second transit epoch is shown). This is the same format as used for theoretical predictions in Paper I and for the observations of HD 209458 in Paper II. For the strong lines, these ratios reach a maximum amplitude of around 1% but rather less for the weak lines. Although qualitatively similar, the quantitative amplitude depends on the intensity gradients in the line flanks; shallower profiles with weaker gradients produce smaller ratios, thus requiring better S/N for full analysis. A number of such synthetic line ratios for different models were in Paper I. In the ratios between our in-transit spectra with \( S/N \sim 2,000 \) and the out-of-transit reference spectrum with \( S/N \sim 5,000 \), noise
levels on the order of 0.001 or slightly better are expected, consistent with the wiggles seen in Fig. 5.

6.6. Rossiter–McLaughlin effect

The overall sinusoidal patterns in Fig. 5 originate mainly from the successively shifting line wavelengths during transit. This modulation of the apparent radial velocity constitutes the Rossiter–McLaughlin effect, usually determined by cross-correlating the full stellar spectrum but here we can extract it for specific spectral lines from wavelength fits during the various transit epochs (Fig. 6). Although such line-center fits to Fe i lines need not give identical values to those obtained from cross-correlations over entire spectra, the similarity to the measured Rossiter–McLaughlin effect in Alopex (e.g., Winn et al. 2006) serves to confirm the integrity of the present data reductions.

However, these measured values only show relative velocities. As illustrated by various theoretically modeled Rossiter–McLaughlin curves in Paper I, a lot of additional information could be extracted if such curves could be obtained on an absolute wavelength scale and also separately for different types of spectral lines. That endeavor will require very accurate laboratory wavelengths for many lines but appears feasible to attempt with data not much superior to the present set.

In a related but different approach, Collier Cameron et al. (2010) used observations of Alopex to model the velocity cross-correlation function of the stellar spectrum to identify spectral-line distortions across the surface of the star during transit, deducing the trajectory of the missing starlight (“Doppler shadow”) and obtaining measures of the projected stellar rotation rate and geometry.

7. Spatially resolved line profiles

The normalized spectral flux \( S \) behind the effective planetary area \( A_{\text{eff}} \) is obtained as \( (S_{\text{out-transit}} - S_{\text{in-transit}})/A_{\text{eff}} \), while the steps in reconstructing continuum-normalized spatially resolved profiles were described in Paper II (e.g., its Fig. 9). Such profiles obtained from the strong- and weak-line averages are shown reconstructed at various stellar disk positions in Figs. 7 and 8. These are for the transit epochs 2–9, where the nominal S/N in the reconstructed profile intensities near mid-transit is around 35, falling to \( \sim 20 \) at the beginning and end.

Since the reconstructions involve dividing subtracted spectra (with noise \( \leq 10^{-3} \) of the continuum) by the small values of \( A_{\text{eff}} \) (Fig. 1), the noise is correspondingly enhanced. Closer to disk center, \( A_{\text{eff}} \) reaches values of \( \sim 0.025 \), enabling S/Ns on the order of 30. However, at the near-limb positions at epochs 1 and 10, \( A_{\text{eff}} \) drops to very small values. Those profiles attain much lower S/N and are not shown. Measuring near-limb positions is hard both because the star is substantially limb darkened and the planet is already partially outside the stellar disk.

7.1. Stellar rotation

Not being subject to stellar rotational broadening, spatially resolved line profiles are deeper and narrower than the integrated profile from the full disk. The stellar rotation is known previously from both measured line broadening and from the Rossiter–McLaughlin effect but can be verified anew. The gradual shift of the central wavelength shows the amount of stellar rotation at the latitude of the transit chord, while the shift from a relative blueshift on the ingress side of the transit, to a redshift on the egress side confirms the prograde orbital motion of the planet relative to stellar rotation (Figs. 7–8; 10).

The apparent latitude of transit is known to be \( \sim 34^\circ \); the tilt of the stellar rotational axis seems consistent with the stellar being aligned with the planetary orbit (Henry & Winn 2008). The velocity shift of \( \sim 3 \text{ km s}^{-1} \) observed across the (partially measured) planetary transit chord at a latitude where the projected stellar rotational velocity equals \( \cos 34^\circ \approx 0.8 \) times the equatorial value, is consistent with various previous determinations indicating a comparable value for \( V \sin i \) but would need improved data with higher spectral resolution to be better constrained.

7.2. Fitted line parameters

In addition to the reconstructed line profiles at different epochs, Figs. 7 and 8 also show Gaussian fits to these profiles.
Fig. 7. Reconstructed line profiles (bold dashed) for the strong Fe i line at eight positions during the planetary transit, and Gaussian fits (thin solid). Spatially resolved profiles are not subject to rotational broadening and are deeper and narrower than the disk-integrated profile outside transit shown at bottom. The successive transition from blue- to red-shift shows the prograde orbital motion of the planet relative to stellar rotation. By averaging over the remaining noise, such fits provide parameters of the overall line profiles, which are shown in Fig. 10. Line-bottom intensities are in units of the local spectral continuum at each $\mu$, while the line widths are obtained from five-parameter fits to modified Gaussian functions of the type $y_0 + a \cdot \exp[-0.5 \cdot (|x - x_0|/W)^2]$, yielding $W$ as a line-width measure. It is not suggested that the profiles would be intrinsically Gaussian, but such were found to give better fits than, for example, Lorentzian profiles. These changes such as in fitted line-widths and line-bottom intensities can then be compared to theoretical expectations.

Fig. 8. Reconstructed line profiles for the weak Fe i line at eight positions during the planetary transit, analogous to Fig. 7. Time increases from bottom up, and the planet positions for the successive transit epochs (left to right) corresponding to each line profile are to scale.
Figure 9 shows synthetic line profiles from a 3D model of a K-dwarf photosphere (for modeling details, see Paper I). Limb darkening is pronounced in these cooler stars, adding to the challenges of reconstructing line profiles close to the limb. It can be noted that the strongest among these synthetic lines develops pronounced damping wings, while the shapes of the weaker lines are more Gaussian-like. Our observational samples do not include any really strong lines. In the initial scrutiny of the spectrum, a few such lines were identified as candidates but were not retained because their profiles were clearly outside the distribution in Fig. 4, while their few numbers would not permit us to reach meaningful S/Ns.

One center-to-limb signature that may be expected from the structure of solar-like granular convection comes from horizontal velocities in the photosphere generally being greater than vertical velocities. Rising gases from below decelerate and turn over on heights comparable to the vertical pressure scale height, which is rather smaller than the horizontal extent of granules, and thus horizontal velocities must be greater to satisfy mass conservation. Line widths would then show a characteristic increase toward the limb, where the greater horizontal motions contribute more Doppler broadening. Such a gradual broadening is well known for the Sun (e.g., Lind et al. 2017), and was also indicated by the spatially resolved spectra across the G0 V star HD 209458 in Paper II. However, no such effect is seen in the results of Fig. 10 (at least within the range of observed μ).

7.3. Spectrometer resolution

Limitations in how rigorous analyses that can be carried out are set by not only the residual noise levels, but also by the finite spectral resolution and the imperfectly known spectrometer response function. The exact instrumental profile of HARPS and its ensuing spectral resolution depend somewhat on the exact arrangement of the fiber that is feeding light into the spectrometer but is nominally \( \lambda/\Delta \lambda \approx 115,000 \), i.e., \( \sim 2.6 \text{ km s}^{-1} \) (Mayor et al. 2003; Rupprecht et al. 2004; ESO 2018). This value refers to the full width at half maximum, which in the spectrometer is sampled by about four detector pixels.

When comparing to synthetic stellar profiles that are computed with much higher resolution, an appropriate correction has to be applied. This correction implies a decrease of the observed line-width measures in Fig. 10 by \( \sim 1.0 \text{ km s}^{-1} \) for the strong lines, and \( \sim 1.2 \text{ km s}^{-1} \) for the weak ones. Even then, the line widths would be slightly broader than their intrinsic values since another broadening arises from the spatial smearing across the stellar disk introduced by the averaging of a few sequential exposures.

8. Theoretical 3D simulations

With currently achievable precision, comparisons to synthetic line profiles mainly have to be against their overall properties such as line widths or depths, rather than more subtle asymmetries or the dependence on excitation potential. To understand what signatures may be realistically detected by studies such as this work, such integral properties were examined for synthetic line profiles of main-sequence stars representing spectral types F, G, and K. These are from our grid of CO \(^5\)BOLD model atmospheres (Freytag et al. 2012) in the temperature range between \( T_{\text{eff}} = 3960 \) and 6730 K, as described in Paper I.

No model in this grid has parameters precisely corresponding to those of Alopex, but it is bracketed by the models for 5900 K (\( \sim \)G0 V) and 3960 K (\( \sim \)K8 V), both with solar metallicity and surface gravity \( \log g \) [cgs] = 4.5. Some earlier modeling of line profiles from 3D models with parameters close to Alopex were made by Dravins & Nordlund (1990b) and Ramirez et al. (2009), but those did not then foresee comparisons to spatially resolved spectroscopy.

In Fig. 11, the center-to-limb behavior of line widths, strengths, and shifts are shown for differently strong lines from various models. As before, line-width measures are obtained...
from five-parameter fits to modified Gaussians while line-bottom intensities are in units of the local (limb-darkened) spectral continuum at each \( \mu \). Line-shift values obtained from symmetric Gaussian fits do not resolve asymmetric signatures such as bisector shapes, i.e., the varying line shifts at different depths in the line. The convective line shifts are absolute (i.e., relative to the stellar frame of rest) but gravitational redshifts are neglected. Similar to Paper I, calculations are made assuming local thermodynamic equilibrium for Fe i lines with wavelength \( \lambda = 620 \text{ nm} \) and lower excitation potential \( \chi = 3 \text{ eV} \).

In general, line widths are expected to increase toward the limb, where the greater horizontal motions should contribute more Doppler broadening. However, the different surface structure of granulation in hotter and cooler stars strongly modifies the center-to-limb changes in line parameters, in particular those of the line width. The vigorous granulation in hotter F-type stars is predicted to be naked, i.e., with full temperature and velocity contrasts directly visible across their corrugated optical-depth surfaces (Allende Prieto et al. 2002; Chiavassa et al. 2018; Dravins & Nordlund 1990a,b). For example, the convective blueshift is predicted to increase from disk center toward the limb, where many spectral contributions come from horizontal flows on the sloping hills facing the observer. These approaching flows are blueshifted while the equivalent redshifted components remain invisible behind these hills and an enhanced blueshift results. This also exposes the full amplitude of the horizontal velocity field to an outside observer, causing a correspondingly greater line broadening.

On solar-like G-type stars, the brightness and velocity amplitudes of granulation are slightly veiled beneath the line-forming layers. As a consequence, the brightness contrast decreases with height, manifest in effects such as a clear dependence of convective blueshift on line strength and its decrease from disk center toward the limb. In cooler K-type stars such as Alopex, however, the expected contrast of granulation that is visible on the surface is substantially lower than for the Sun or hotter stars since the granulation structures are more strongly veiled beneath the visible surface. The fully developed contrast of granulation is not strictly a surface phenomenon in this case, but rather relates to those slightly deeper layers in which the energy flux changes from being mainly convective to mainly radiative. Although this hidden granulation is not deep down in terms of linear depth – maybe only some 100 km – the corresponding optical depths are substantial for spectral line formation, and emerging line profiles are expected to carry but modest signatures of the convection in deeper layers (Chiavassa et al. 2018; Dravins & Nordlund 1990b; Magic et al. 2013; Nordlund & Dravins 1990; Ramírez et al. 2009; Tremblay et al. 2013). As a consequence, cool K stars are expected to produce only minimal center-to-limb changes in line widths (Fig. 11), which is consistent with the lack of any corresponding observed signature in Fig. 10.

With spectral lines only slightly affected by granulation, their variability due to changes in granulation must be expected to be small as well, and the ensuing tiny photometric and spectral microvariability appear to make such stars prime candidates in searches for Earth-analog exoplanets, for which the stellar microvariability is a limiting factor in hotter stellar hosts (at least as long as effects from magnetic activity, common in the coolest stars, do not become dominant).

9. Outlook and future potential

This work now extends the number of stars with high-resolution photospheric spectra across their surfaces to a total of three (including the Sun), and the experience gained in understanding what noise levels can realistically be reached, may guide the planning of future observations. This work used different types of spectroscopic data compared to the study of HD 209458 in Paper II. The wavelength stability of current HARPS spectra removed the need for such elaborate wavelength calibrations that were required for UVES spectra in Paper II. Current data
Fig. 11. Center-to-limb changes of overall parameters for differently strong lines computed from the various CO BOLD models representing stars of spectral types F, G, and K. Properties of strong lines are shown by solid curves, of intermediate lines by long-dashed, and of weak lines by short-dashed curves. Line-width measures, line-center intensities, and convective line shifts are from symmetric Gaussian fits to the full synthetic profiles and therefore do not resolve any line asymmetries. Convective line shifts are in absolute units but gravitational redshifts are neglected.

9.1. Limitations in spectral-line averaging

Present types of studies may ultimately be constrained by the number and types of spectral lines that actually are present in stellar spectra. Even if theoretical models permit the precise calculation for lines of some particular strength, excitation potential, and ionization level from various atomic species, comparisons to observations may be unfeasible if real stars would not possess such spectral lines in sufficient numbers.

Simulations were used to examine how extensive the averaging can be while simultaneously remaining valid, i.e., that the averaged line profile remains representative of a line whose strength and excitation potential are similar to that of the line-group average. Figure 9 shows profiles from a model of a cool dwarf for three different line strengths at four different center-to-limb positions. For a hotter model, profiles for five different line strengths were in Fig. 2 of Paper I, while Fig. 4 of that paper showed the excitation-potential dependence for different solar lines. In all models – at least for lines of moderate strength – there is a continuous and smooth change of line shapes, such that the average of slightly stronger and slightly weaker line shapes (or such of slightly different excitation potentials) indeed closely agree with the profile of an intermediate-parameter line.

However, this smooth variation does not hold for the very strongest lines, which start to develop distinctive damping wings, and for such lines a separate treatment is called for. As mentioned above, a few such very strong and also reasonably unblended lines were identified in the spectrum of Alopex but they were too few to permit averaging to sufficiently high S/N. Also, the very weakest lines would merit a separate treatment, although their analyses will require lower noise spectra than presently available.

The range of line strengths for which such averaging is valid decreases for more subtle line parameters such as asymmetries and bisector shapes. This was illustrated with synthetic bisectors in Figs. 5–7 of Paper I. Averaging will still be valid but has to be restricted to lines of a more limited parameter spread. While not attempted in this work, searches for bisector dependence should become feasible with future data. Also, averaging of lines from different species (Fe i, Fe ii, Ti i, Ti ii, etc.) would give access to a larger sample of photospheric lines with rather similar diagnostic potential, as seen in line-group averages from spectra of the Sun and Procyon (Dravins 2008).

9.2. Challenges in high-fidelity spectroscopy

Clearly, these types of studies critically depend upon achieving the very best S/N levels. Even if many recordings can (and must) be averaged, such stacking typically only reduces the random
noise as the square root of the number of exposures, a slowly growing function. For efficiently probing stellar surfaces, spectra with initial S/Ns on the order of 500 or more will be required, such that are becoming available with high-performance instruments such as PEPSI on LBT (Strassmeier et al. 2015, 2018a,b) or ESPRESSO on the ESO VLT (Pepe et al. 2014; González Hernández et al. 2017).

Although various 3D atmospheric signatures are potentially observable in spatially resolved stellar spectra, achievable S/N limits the more realistically measurable quantities to the center-to-limb changes of entire line profiles, such as their overall widths and depths. As illustrated in Fig. 11, even such quantities may strongly depend on the surface granulation structure, and the center-to-limb variation in line-widths are predicted to be drastically greater in hotter F-type stars than the cooler K-types. Fig. 12 shows these line-profile changes in more detail. To verify such predictions requires observations of some suitably bright stars with large transiting planets. The two planet host stars now analyzed in Papers II and III were selected for their apparent brightness and planet size (Fig. 1 in Paper II). However, ongoing searches for bright host stars with transiting exoplanets keep finding new targets, a recent discovery being a hot Jupiter transiting the $m_V = 7.6, \text{ rapidly rotating A2 V star HD 185603 with an } 0.81\% \text{ transit depth (Lund et al. 2017). Such a } T_{\text{eff}} \sim 8730 \text{ K star may have fewer measurable lines and pose other challenges but is just one example of a target for which spatially resolved stellar spectroscopy could explore new parameter domains of stellar astrophysics.}

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Appendix A: Listing of lines

List of the 158 largely unblended Fe i lines selected; 86 weaker lines (measured absorption-line central intensity ≥55% of continuum) and 72 stronger lines. Wavelengths and excitation potentials are from Stenflo & Landegren (1977); line-center intensities are in units of the normalized local continuum as obtained from averaged Gaussian fits to all current HARPS exposures. These intensities are measured values, and have been subject to convolution with the spectrometer instrumental profile; observations with higher spectral resolution would yield deeper lines. A graphical display of these sets of lines is in Fig. 2.

Table A.1. Selected weaker Fe i lines.

| Wavel. (nm) | Int. (%) | Exc. pot. (eV) | Wavel. (nm) | Int. (%) | Exc. pot. (eV) | Wavel. (nm) | Int. (%) | Exc. pot. (eV) |
|------------|---------|---------------|------------|---------|---------------|------------|---------|---------------|
| 455.16499  | 62      | 3.94          | 553.92824  | 79      | 3.64          | 616.53641  | 61      | 4.14          |
| 459.35268  | 61      | 3.94          | 555.26919  | 91      | 4.95          | 622.67403  | 71      | 3.88          |
| 465.78579  | 55      | 2.84          | 556.88689  | 86      | 3.63          | 631.15050  | 68      | 2.83          |
| 465.82976  | 72      | 3.27          | 560.76668  | 83      | 4.15          | 631.58164  | 63      | 4.07          |
| 467.28364  | 59      | 1.61          | 561.13587  | 86      | 3.63          | 638.07483  | 59      | 4.19          |
| 472.61396  | 73      | 3.00          | 561.86360  | 55      | 4.21          | 638.57206  | 88      | 4.73          |
| 478.59583  | 67      | 4.14          | 563.58247  | 65      | 4.26          | 639.25429  | 73      | 2.28          |
| 479.43571  | 76      | 2.42          | 563.66992  | 74      | 3.64          | 643.64102  | 88      | 4.19          |
| 479.94092  | 58      | 3.64          | 564.66854  | 90      | 4.26          | 649.64738  | 57      | 4.79          |
| 480.25216  | 81      | 4.61          | 565.14716  | 79      | 4.47          | 657.42325  | 57      | 0.99          |
| 480.81509  | 60      | 3.25          | 565.23194  | 72      | 4.26          | 658.12143  | 71      | 1.48          |
| 480.99400  | 70      | 3.57          | 566.13480  | 75      | 4.28          | 660.83010  | 74      | 2.28          |
| 521.38071  | 88      | 3.94          | 567.76875  | 90      | 4.10          | 662.75488  | 76      | 4.55          |
| 522.31851  | 63      | 3.63          | 568.02441  | 86      | 4.19          | 664.69355  | 85      | 2.61          |
| 523.62039  | 65      | 4.19          | 572.08950  | 83      | 4.55          | 670.35720  | 62      | 2.76          |
| 529.39609  | 67      | 4.14          | 579.39178  | 66      | 4.22          | 671.03213  | 74      | 1.48          |
| 529.45493  | 79      | 3.64          | 580.77868  | 89      | 3.29          | 673.79830  | 82      | 4.56          |
| 535.81168  | 84      | 3.30          | 581.19172  | 86      | 4.14          | 673.95243  | 78      | 1.56          |
| 538.63345  | 64      | 4.15          | 581.48092  | 75      | 4.28          | 674.59626  | 92      | 4.07          |
| 539.52187  | 77      | 4.44          | 582.78794  | 84      | 3.28          | 674.69508  | 92      | 2.61          |
| 541.70405  | 65      | 4.41          | 583.51018  | 84      | 4.26          | 675.27107  | 74      | 4.64          |
| 546.08762  | 88      | 3.07          | 585.22222  | 64      | 4.55          | 679.32656  | 87      | 4.07          |
| 546.15530  | 71      | 4.44          | 585.87840  | 85      | 4.22          | 680.68491  | 64      | 2.73          |
| 546.42825  | 63      | 4.14          | 586.11123  | 90      | 4.28          | 682.03730  | 69      | 4.64          |
| 547.09957  | 71      | 4.44          | 588.12822  | 84      | 4.61          | 682.85976  | 61      | 4.64          |
| 548.71489  | 67      | 4.41          | 590.24755  | 85      | 4.59          | 683.98340  | 67      | 2.56          |
| 549.18346  | 85      | 4.19          | 592.96802  | 65      | 4.55          | 684.13450  | 60      | 4.61          |
| 549.35012  | 65      | 4.10          | 603.40365  | 90      | 4.31          | 684.36060  | 59      | 4.55          |
| 552.24491  | 58      | 4.21          | 608.27147  | 59      | 2.22          |
### Table A.2. Selected stronger Fe\textsc{I} lines.

| Wavel. (nm) | Int. (%) | Exc. pot. (eV) | Wavel. (nm) | Int. (%) | Exc. pot. (eV) | Wavel. (nm) | Int. (%) | Exc. pot. (eV) |
|------------|----------|----------------|------------|----------|----------------|------------|----------|----------------|
| 436.59004  | 37       | 2.99           | 525.06527  | 26       | 2.20           | 602.70562  | 49       | 4.07           |
| 443.25726  | 39       | 3.57           | 525.34693  | 36       | 3.28           | 605.60114  | 49       | 4.73           |
| 444.54760  | 33       | 0.09           | 536.54063  | 38       | 3.57           | 606.54921  | 29       | 2.61           |
| 452.34015  | 47       | 3.65           | 536.74755  | 29       | 4.41           | 615.16217  | 50       | 2.18           |
| 457.42191  | 48       | 3.21           | 536.99702  | 30       | 4.37           | 615.77331  | 52       | 4.07           |
| 460.20006  | 24       | 1.61           | 537.37136  | 48       | 4.47           | 617.33433  | 43       | 2.22           |
| 467.88519  | 23       | 3.60           | 537.95796  | 44       | 3.69           | 618.02084  | 51       | 2.73           |
| 474.15341  | 29       | 2.83           | 538.94866  | 38       | 4.41           | 620.03204  | 41       | 2.61           |
| 483.95500  | 39       | 3.27           | 543.29525  | 46       | 4.44           | 621.34375  | 36       | 2.22           |
| 487.43565  | 64       | 3.07           | 544.50502  | 34       | 4.39           | 621.92886  | 35       | 2.20           |
| 487.58815  | 40       | 3.33           | 547.39076  | 40       | 4.15           | 623.26493  | 43       | 3.65           |
| 488.54361  | 35       | 3.88           | 552.55472  | 53       | 4.23           | 626.51412  | 35       | 2.18           |
| 489.28624  | 50       | 4.22           | 554.39399  | 49       | 4.22           | 627.02322  | 52       | 2.86           |
| 490.93874  | 42       | 3.93           | 563.82675  | 41       | 4.22           | 629.78013  | 40       | 2.22           |
| 491.80152  | 51       | 4.23           | 566.25233  | 37       | 4.18           | 632.26936  | 41       | 2.59           |
| 494.63941  | 26       | 3.37           | 570.15527  | 34       | 2.56           | 633.53378  | 33       | 2.20           |
| 495.01108  | 34       | 3.42           | 570.54677  | 63       | 4.30           | 640.80262  | 42       | 3.69           |
| 498.32566  | 31       | 4.15           | 571.78379  | 51       | 4.28           | 643.08538  | 32       | 2.18           |
| 504.42164  | 34       | 2.85           | 573.17666  | 51       | 4.26           | 648.18784  | 46       | 2.28           |
| 509.07807  | 35       | 4.26           | 575.31287  | 43       | 4.26           | 649.89461  | 49       | 0.96           |
| 514.17460  | 26       | 2.42           | 577.50849  | 50       | 4.22           | 659.38798  | 39       | 2.43           |
| 524.24988  | 31       | 3.63           | 591.62535  | 47       | 2.45           | 660.91189  | 47       | 2.56           |
| 524.37823  | 45       | 4.26           | 595.66997  | 41       | 0.86           | 675.01597  | 43       | 2.42           |
| 525.02171  | 29       | 0.12           | 600.79656  | 54       | 4.65           | 685.51684  | 54       | 4.56           |