The benefits of absorption enhancement in an optical cavity were appreciated shortly after the invention of the laser [1]. The effective interaction length increases as a consequence of beam trapping inside a stable resonator. Techniques such as cavity ring-down spectroscopy exploit this effect to achieve $10^{-10}$ absorption sensitivity in gaseous media [2, 3]. Broadband spectroscopy can be performed with the cavity ring-down concept by means of an optical frequency comb [4]. The high sensitivity achieved with gases is possible because of the low intrinsic absorption and minimal parasitic losses.

Use of an optical cavity in condensed matter spectroscopy is usually not necessary because of the larger absorption. There are applications, however, that can benefit from placing a weakly absorbing solid-state medium in an optical resonator. Resonantly enhanced absorption has been shown to increase the electronic bandwidth of infrared detectors and provides spectral tuning of the response [5]. Here we use an optical cavity to increase pump light absorption in experiments to optically refrigerate glass.

Laser cooling in solids occurs by anti-Stokes luminescence, i.e. conversion of coherent pump photons into isotropic, higher energy luminescence photons [6, 7]. The energy gained in the luminescence process is supplied by phonon absorption. If excited state relaxation is predominantly radiative, net cooling of the high purity medium occurs. In 1995, Epstein et al demonstrated net laser cooling in solids for the first time by using high purity fluoro-zirconate glass (ZBLAN) that had minimal non-radiative losses [8]. Since then, a variety of solid hosts, both amorphous and crystalline, doped with rare-earth ions of ytterbium (Yb), thulium, and erium have been cooled by laser light [9, 10]. The cooling power (i.e. rate of heat lift) of an optical refrigerator is

$$ P_{\text{cool}} = P_{\text{abs}}(\eta \nu_F / \nu - 1), $$

where $P_{\text{abs}}$ is the absorbed optical power, $\nu$ is the pump frequency, $\nu_F$ is the mean fluorescence frequency, and $\eta$ is the external quantum efficiency that accounts for photon emission and escape [11]. To attain net cooling (i.e. $P_{\text{cool}} > 0$), pumping must take place at frequencies smaller than the mean luminescence frequency. This is where absorption is inherently weak, however, which makes $P_{\text{abs}}$ very low.

Pump absorption can be improved by increasing the interaction length with a multi-pass scheme. A non-resonant trapping geometry places the sample between two dielectric mirrors with pump light admitted through a small entrance hole in the input mirror. This approach led to cooling by 90 degrees starting from room temperature in Yb:ZBLAN glass [12]. Much lower temperatures have been recently attained with a Yb-doped yttrium-lithium fluoride crystal host using both resonant and non-resonant absorption enhancement [13, 14].

We use an optical cavity to dramatically enhance pump light absorption in a Yb:ZBLAN glass sample. Resonant cavity enhancement (RCE) offers the benefits of increased interaction length without complications associated with the entrance hole in a multi-pass setup, i.e. pump light scatter and heating, as well as pump light leakage from the trap. The sample is positioned between two mirrors to form a stable cavity as shown in Fig. 1a. The maximum absorption of the resonant cavity occurs when the reflectivity of the input mirror ($I$) satisfies $R_I = R_B \exp(-2\alpha L)$, where $R_B$ is the back mirror reflectivity, and $\alpha$ is the absorption coefficient of the glass sample of length $L$ [5]. Parasitic (background) loss is ignored. The equation expresses optical impedance matching for a lossy cavity [15].

In a Gires-Tournois cavity geometry, the back mirror reflectivity $R_B$ is taken as unity and the pump absorption on resonance is given by
When the optical impedance matching condition is satisfied in the Gires-Tournois limit, absorption goes to unity.

The sample used in this work is much longer than a pump wavelength, i.e. $2nL/\lambda \gg 1$ so positioning in the cavity is not critical. In a thin detector application, where the active element is of the order of a wavelength thick, it must be located at an anti-node of the cavity standing wave [16]. We also note that the cavity pumping scheme can be implemented by placing an optically cooled sample directly inside a laser resonator [17]. This approach is complicated by the fact that the temperature-dependent round-trip loss of the sample will affect the lasing threshold.

Referring to Figure 1a, the pump field is derived from a commercial continuous-wave Yb:YAG disk laser (ELS Versadisk) nominally oscillating at 1030 nm. After passing through a pair of Faraday isolators (60 dB combined rejection) and spatial mode-matching lens pair, the pump beam enters an optical cavity placed inside a vacuum chamber. The cooling sample (S) is fluoro-zirconate glass ZBLAN (ZrF$_4$-BaF$_2$-LaF$_3$-AlF$_3$-NaF) doped with 2% w.t. Yb$^{3+}$. It is cylindrical in shape, length: 1 cm length, and diameter: 1 cm, which is similar to the sample used in Ref. [12]. A high-quality dielectric mirror is deposited on the back facet; the front facet is anti-reflection coated at the pump wavelength ($R_{AR} < 0.2\%$). The sample is supported by quartz optical fibers to minimize conductive heat load from the environment. The radiative load can be reduced by nearly 6 times by placing the sample inside a shell coated with low thermal emissivity film on its interior surfaces [12]. In this work, a partial shell is used to allow thermal camera access for non-contact temperature measurements described below. We estimate the partial shell provides about half the radiation shielding of a full shell. An input coupling mirror (I) of reflectivity $R_I = 94\%$ is housed in a 3-axis piezo-actuated mount, allowing for cavity length scan and stabilization. This reflectivity is chosen to satisfy optical impedance matching with the sample starting at room temperature. The transmission of the back mirror is $T_B < 0.1\%$, consistent with the Gires-Tournois geometry. Losses at both $T_B$ and $R_{AR}$ are negligible compared to the sample single-pass absorbance ($4.5 \pm 0.5\%$), ensuring that absorption enhancement is largely in the sample. For the measured values of $R_I$ and $\alpha L$, the calculated on-resonance absorption (Eq. 1) lies in the range $96.5 \pm 2\%$.

A reflectivity signal ($R$) is used to estimate the resonant absorption of the Gires-Tournois cavity. Normalization is obtained from a high-reflectivity dielectric mirror placed immediately before the input coupler ($R_I$). Since transmission is negligible in the Gires-Tournois geometry, we deduce absorption $A$ from energy conservation: $A = 1 - R$ while ignoring interface and scattering losses. The experimental on-resonance absorption of $89 \pm 3\%$ is shown in Fig. 1b. This result is in good agreement with the theoretical prediction, which is reduced from the nominal value of $96.5 \pm 2\%$ by imperfect mode-matching as evidenced by fringe asymmetry in the reflectivity signal.

The cavity is kept on resonance with an active stabilization scheme. Laser-induced isotropic luminescence is fiber-coupled into a photo detector ($F$) and used as an error-generating signal for the feedback loop. The cavity length is modulated by a small-amplitude voltage from the internal reference of a lock-in amplifier. By mixing luminescence and dither voltage signals in a lock-in filter it is possible to differentiate the leading and trailing edges of a cavity fringe. This allows generation of an unambiguous directional feedback signal via a proportional-integral-derivative (PID) circuit (SRS, Model SIM960).

Laser cooling experiments are performed by irradiating the sample with 2 Watts of pump laser light. The black-body radiation emitted by the sample is imaged onto a micro-bolometer thermal camera, thus providing a non-contact scene temperature measurement. Averaged pixel counts from a time series of thermal images are converted to temperature by means of a calibration coefficient obtained in a separate experiment. The time evolution of temperature is presented in Figure 2. A thermal image is shown in the inset corresponding to resonant cooling by 3 degrees below the temperature of the adjacent radiation shell. The cooling process is terminated by blocking the laser 60 minutes into the experiment to avoid saturation of the thermal camera image. Exponential fitting of the cooling data extrapolates to a steady state temperature decrease of 5 degrees below the shell temperature.

When account is made for non-ideal experimental conditions, our results compare favorably with the nearly 45 degrees of cooling reported at the same pump power and in a non-resonant arrangement [12]. If we adjust absorption efficiency (90%), current cavity stabilization efficiency (60%), and radiation shielding (30%) to their ideal values, a temperature drop of 30 K from ambient
is predicted. Stabilization efficiency is limited by longitudinal mode instability of the pump laser. Sample-to-sample impurity variations can account for the remaining performance discrepancy [18].

An important advantage of RCE compared to non-resonant trapping schemes is its scalability. Cavity mode-volume and hence sample size can be matched in an RCE absorption arrangement. The dominant parasitic load is radiative, which scales linearly with sample surface area. Reducing the mode-volume along with sample dimensions will improve laser cooling performance. An added benefit will be miniaturization of the cryocooler.

The above proof-of-principle experiment demonstrates the feasibility of RCE in laser cooling of solids. For large temperature excursions (i.e. to reach cryogenic temperatures), dynamic optical impedance matching becomes an important consideration. Due to the temperature-dependent absorption coefficient, total absorption $A$ in a fixed cavity can be maximum only at a particular temperature. Optimal coupling requires that the input mirror reflectivity $R_1$ change to accommodate the change in the intra-cavity loss. A work-around solution is to undercouple the cavity at room temperature so as to satisfy impedance matching at a lower, steady-state temperature $T'$, where $α(T')$ is known. A more general solution is to implement a continuously tunable reflectivity. This concept was recently demonstrated in fiber-based cavity, where input reflectivity was tuned by an adjustable evanescent coupling loss in the input fiber [19]. Here, we propose a free-space optics solution in the form of a coupled cavity geometry to allow for active impedance matching.

Without loss of generality, consider a symmetric cavity of reflectivity $R_1$ followed by an absorbing sample and a third mirror $R_2$. The half-round trip phases of the first (coupling) and second (absorbing) sub-cavities are $φ_{1,2}$. Within the adiabatic approximation [20], the optical impedance matching condition can be generalized to:

$$R_{11} (φ_1) = \frac{F \sin^2 (φ_1)}{1 + F \sin^2 (φ_1)} = R_2 e^{-2αL}, \quad (2)$$

where $F = 4R_1/(1 - R_1)^2$. Coupling between the two cavities causes Eq. (2) to be satisfied only for a particular value of $φ_2$. Resonant reflectivity of the first (coupling) cavity $(R_{11})$ acts as a tunable input coupler to maximize the absorption. The maximum reflectivity given by Eq. (2) sets the minimum absorbance that allows impedance matching:

$$(αL)_{\text{min}} = \ln \left( \frac{1 + R_1}{2\sqrt{R_1}} \right) \quad (3)$$

for $R_2 = 1$. The case of interest here involves small values of $αL$, so the minimum reflectivity $R_1$ that satisfies the optical impedance matching condition is $R_1 ≈ 1 - \sqrt{8αL}$. This means that a range of intra-cavity loss values can be actively impedance matched by the input coupling cavity. To satisfy optical impedance matching for $αL ≈ 10^{-9}$, a reflectivity of $R_1 ≥ 0.9999$ is required. When the resonant absorption is extremely small, however, losses at the cavity mirrors can no longer be ignored in the analysis.

The proposed technique of optical impedance matching via a coupled cavity geometry is general. We envision several potential applications outside of laser cooling in solids. Background-free, narrow-band, ultra-sensitive spectroscopy is possible, where an acoustic signal proportional to weak absorbance can be monitored as a function of sub-cavity phases.

In summary, we used a resonant cavity to obtain nearly 90% absorption in a laser cooling sample, corresponding to 20-fold enhancement over single-pass absorbance. A 5 degree temperature drop from the ambient was shown to be comparable to the performance of state-of-the-art glass-host coolers when accounting for experimental inefficiencies. We propose and outline a coupled cavity scheme to achieve active optical impedance-matching in high-power laser cooling experiments.

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