How to Estimate the Far-Side Open Flux Using STEREO Coronal Holes

Stephan G. Heinemann1 · Manuela Temmer2 · Stefan J. Hofmeister3 · Aleksandar Stojakovic2 · Laurent Gizon1,4,5 · Dan Yang1

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Abstract
Global magnetic field models use as input synoptic data, which usually show “aging effects” as the longitudinal 360° information is not obtained simultaneously. Especially during times of increased solar activity, the evolution of the magnetic field may yield large uncertainties. A significant source of uncertainty is the Sun’s magnetic field on the side of the Sun invisible to the observer. Various methods have been used to complete the picture: synoptic charts, flux-transport models, and far side helioseismology. In this study, we present a new method to estimate the far-side open flux within coronal holes using STEREO EUV observations. First, we correlate the structure of the photospheric magnetic field as observed with the Helioseismic and Magnetic Imager on board the Solar Dynamics Observatory (HMI/SDO) with features in the transition region. From the 304 Å intensity distribution, which we found to be specific to coronal holes, we derive an empirical estimate for the open flux. Then we use a large sample of 313 SDO coronal hole observations to verify this relation. Finally, we perform a cross-instrument calibration from SDO to STEREO data to enable the estimation of the open flux at solar longitudes not visible from Earth. We find that the properties of strong unipolar magnetic elements in the photosphere, which determine the coronal hole’s open flux, can be approximated by open fields in the transition region. We find that structures below a threshold of 78% (STEREO) or 94% (SDO) of the solar disk median intensity as seen in 304 Å filtergrams are reasonably well correlated with the mean magnetic flux density of coronal holes (\(\ccsp = 0.59\)). Using the area covered by these structures (\(A_{OF}\)) and the area of the coronal hole (\(A_{CH}\)), we model the open magnetic flux of a coronal hole as 
\[
|\Phi_{CH}| = 0.25A_{CH} \exp(0.032A_{OF})
\]
with an estimated uncertainty of 40 to 60%.

Keywords Corona · Coronal holes · Magnetic field · Open flux

✉ S.G. Heinemann
stephan.heinemann@hmail.at

1 Max-Planck-Institut für Sonnensystemforschung, Justus-von-Liebig-Weg 3, 37077 Göttingen, Germany
2 Institute of Physics, University of Graz, Universitätsplatz 5, 8010 Graz, Austria
3 Columbia Astrophysics Laboratory, Columbia University, New York, USA
4 Institut für Astrophysik, Georg-August-Universität Göttingen, 37077 Göttingen, Germany
5 Center for Space Science, NYUAD Institute, New York University Abu Dhabi, Abu Dhabi, UAE
1. Introduction

The complex solar magnetic field is usually thought of as an interplay of open and closed fields from the smallest spatial scales up to global scales. The portion of the magnetic field that affects interplanetary space is called open, i.e., the fields close far away from the Sun. Most open fields, and the resulting open flux, are supposed to originate in large-scale magnetic structures known as coronal holes. These coronal holes are usually observed in the solar corona as regions of reduced emission in high-temperature wavelengths such as extreme ultraviolet (EUV) or X-ray (see the review by Cranmer, 2009, and references therein). Along the open field, plasma is accelerated to speeds up to \( \approx 800 \text{ km s}^{-1} \). These plasma outflows are known as high-speed solar wind streams and are the leading cause of minor to moderate geomagnetic activity at distances of 1 AU (Wilcox, 1968; Farrugia, Burlaga, and Lepping, 1997; Alves, Echer, and Gonzalez, 2006; Vršnak et al., 2017; Richardson, 2018).

Intuitively, we would expect that the gross of the open magnetic flux from the Sun originates in coronal holes; however, comparisons of in situ measurements at 1 AU and remote sensing observation of the Sun have revealed a significant discrepancy in the open flux of more than a factor of two, often referred to as the “open flux problem” (Linker et al., 2017; Lowder, Qiu, and Leamon, 2017; Wallace et al., 2019). There are several reasons for this: underestimation of open flux from individual coronal holes due to the method and data used (Linker et al., 2021); the limitation that only near-side magnetic field observations are available; insufficient knowledge of the magnetic flux originating from the solar poles, that is, polar coronal holes; and open flux possibly not associated with observed coronal holes. Recently launched and future space missions going out of the ecliptic plane, such as Solar Orbiter (Müller et al., 2020) or SOLARIS (Hassler et al., 2020), will shed with their unprecedented observational data more light on the polar regions, particularly their magnetic fields. Nowadays the far-side magnetic flux is estimated using synoptic charts (e.g., Lowder, Qiu, and Leamon, 2017), which only show the magnetic field over multiple days and weeks, flux transport models (e.g., Arge et al., 2010; Hickmann et al., 2015), helioseismic measurements adapted into flux transport modeling (Arge et al., 2013) or by estimating far-side active regions (Liewer et al., 2014). Newer approaches try to use machine learning, utilize helioseismology, or plan to use data from Solar Orbiters Polarimetric and Helioseismic Imager (SO/PHI: Solanki et al., 2020); however, these methods are still in their infancy.

Coronal holes extend from the solar surface up into the corona and interplanetary space, and its magnetic field tracers may be seen in heights above the photosphere. On a global perspective, coronal holes appear as large-scale structures dominated by one polarity, which they retain over their lifetime (Levine, 1982; Wang, Hawley, and Sheeley, 1996; Heinemann et al., 2018, 2020). Their open flux (signed to unsigned flux) varies between 6 and 87% (Hofmeister et al., 2017; Heinemann et al., 2019), the average flux densities are 1–15 Gauss (\( \approx 3 \text{ G} \); Bohlin and Sheeley 1978, 1–7 G; Harvey, Sheeley, and Harvey 1982, 1–5 G; Obridko and Shelting 1989, 3.0 \( \pm \) 1.6 G; Hofmeister et al. 2017 and 2.9 \( \pm \) 1.9 G; Heinemann et al. 2019), and they have a significantly reduced temperature (\( \approx 0.95 \text{ MK} \)) and density (\( \approx 1.5 - 2.5 \times 10^8 \text{ cm}^{-3} \)) in contrast to the surrounding quiet Sun (Warren and Hassler, 1999; Hahn, Landi, and Savin, 2011; Wendeln and Landi, 2018; Saqri et al., 2020; Heinemann et al., 2021). The magnetic fine structure of coronal holes is defined by a very weak background field associated with the insides of supergranular cells and unipolar centers of flux accumulation occurring at the lanes and nodes of the magnetic network (i.e., magnetic elements). These magnetic elements may form open funnels that guide the open magnetic flux and solar wind, or form closed loops with nearby magnetic elements of opposite polarity (Dunn and Zirker, 1973; Berger and Title, 2001; Cranmer, 2009; Hofmeister...
et al., 2019). Wiegelmann and Solanki (2004) showed that a relatively large number of these closed structures exists in coronal holes; however, their average height is lower than in the quiet Sun, most likely due to the canopy-like structure of the opening funnels that inhibits the expansion of the closed loops in height. Therefore the fine scale structure of magnetic field within coronal holes leaves traces in larger heights, which possibly can be identified in observations of the transition region such as He II 304 Å EUV data (e.g., Jin, Harvey, and Pietarila, 2013). The 304 Å line is dominated by He II emission at a peak response temperature of about 50 kK, which images primarily the upper chromosphere and transition region (Lemen et al., 2012). This is also the region where it is believed that the rapid expansion of the coronal funnels takes place, and this makes it possible to reliably study the open and closed fields. Because of this and because the filter is available on both spacecraft used in this study, the 304 Å line is suitable to study the relation between the photospheric magnetic field and the chromosphere/transition region intensity of coronal holes, and thereby to estimate the magnetic flux originating from far-side coronal holes.

In this paper, we propose a concept on how to estimate the far-side flux of the Sun using EUV observations of coronal holes taken by the SECCHI suite (Sun Earth Connection Coronal and Heliospheric Investigation; Howard et al., 2008) on-board the STEREO (Solar TERrestrial RElations Observatories; Kaiser et al., 2008) spacecraft. First, we analyze coronal hole properties in the photosphere and the transition region, and show how the open flux of coronal holes can be estimated in higher layers of the solar atmosphere. Second, we use this relation to derive an estimate of the open flux. For this, we use near-side observations from the Helioseismic and Magnetic Imager (HMI; Schou et al., 2012; Couvidat et al., 2016) and the Atmospheric Imaging Assembly (AIA; Lemen et al., 2012) on board the Solar Dynamics Observatory (SDO; Pesnell, Thompson, and Chamberlin, 2012). After establishing the correlation, we use STEREO coronal holes observed at a relatively small separation angle to Earth to calibrate the relation obtained from SDO data for application on STEREO data. Last, we discuss the physical origin of this relation, the implication for space weather forecast, and the limiting factors of the presented method.

2. Methodology

2.1. Magnetic Flux and EUV

2.1.1. Coronal Holes

First, we relate near-side features of the photospheric magnetic field to the EUV intensity distribution of coronal holes. To derive statistically significant results, we use the coronal holes from the CATCH catalog\(^1\) that contains 707 well-defined nonpolar coronal holes extracted from SDO/AIA 193 Å filtergrams using Collection of Analysis Tools for Coronal Holes (CATCH). The catalog includes coronal hole properties, for example, area, intensity, signed and unsigned magnetic field strength and magnetic flux including uncertainty estimates, and the extracted boundaries. The magnetic properties were derived from 720 s Line-of-Sight (LoS) HMI/SDO magnetograms. To correlate properties of the photosphere to the transition region, we constrain our sample to coronal holes with an area of \(A_{\text{CH}} \geq 2 \times 10^{10}\) km\(^2\), that is, all coronal holes that can be considered medium to large. This yields a statistically significant dataset of 313 coronal holes, distributed between latitudes of \(\pm 60^\circ\), located

\(^1\)See https://vizier.u-strasbg.fr/viz-bin/VizieR-3?-source=J/other/SoPh/294.144/.
close to the central meridian, and covering the time range from 2010 to 2019. A detailed description of the catalog and the tool is given by Heinemann et al. (2019).

We use these 313 coronal holes to derive the intensity distribution in AIA/SDO 304 Å filtergrams. The 304 Å data were prepped to level 1.5 (using the SSWIDL routine aia_prep) and corrected for filter degradation using the routines provided by the instrument team. Additionally, due to the reduced emission from coronal holes and the generally low counts caused by the strongly degraded filter, for every coronal hole, 30 images at a cadence of 12 s (= 6 min) are stacked to increase the signal-to-noise ratio. Further, we correct for limb-brightening using an annulus limb-brightening correction (Verbeeck et al., 2014). Finally, the AIA-304 Å data were coregistered to the coronal hole boundary maps, and the regions of interest were extracted.

2.1.2. Quiet Sun

To investigate the reliability and significance of the correlations found in coronal holes, we use a reference dataset consisting of 657 subfields (sf) of a size of 150" × 150" in quiet Sun regions, defined as areas without active regions, coronal holes, filaments, and filament channels. The quiet Sun regions were selected to be spread over a wide latitudinal range similar to the coronal hole dataset, that is, ±60°, to cover the time period from 2010 to 2019. The 304 Å data were preprocessed analogously to the coronal hole dataset as described in Section 2.1.1. The average magnetic flux density of these regions was derived from 720 s LoS HMI/SDO magnetograms following Hofmeister et al. (2017) and Heinemann et al. (2019), for example, correcting for the LoS observations under the assumption of radial field. We further divide the sample into quiet regions (defined as |Bsf| ≤ 3 G) and plage regions (defined as |Bsf| > 3 G). This reference dataset is used to evaluate whether the correlation found for coronal holes is a general property of the transition region or specific to coronal holes.

2.2. Cross-Correlation to STEREO

To determine the open flux of coronal holes on the solar far-side, we have to relate the AIA/SDO observations to observations taken by EUVI/STEREO. To do so, we use 13 coronal holes, which are visible in SDO, STEREO-A, and STEREO-B, within a few days of each other. The coronal holes were selected between October 2010 and July 2011 when the separation angle between Earth and STEREO was lower than 90° in longitude and SDO was already launched. This spatially close position enables a calibration from SDO to STEREO, as in a first-order approximation the evolution of coronal holes in this time range, especially during low solar activity, can be neglected (Temmer, Hinterreiter, and Reiss, 2018). Heinemann et al. (2020) showed that the signed magnetic flux density changes on average at a rate of 27.3 ± 32.2 mG day⁻¹. From this we derive that the difference in magnetic flux density between SDO, where the magnetic field measurements were taken, and the STEREO observations of the coronal holes is < 0.5 G.

These 13 coronal holes are only partly covered by the CATCH catalog for the SDO observations and not covered for STEREO observations. Therefore we detect and extract the coronal holes using CATCH (Heinemann et al., 2019) on 193 Å (AIA/SDO) and 195 Å (EUVI/STEREO) filtergrams. The magnetic field information was again derived from 720 s LoS HMI/SDO magnetograms as described in Section 2.1.2. The EUV intensity distributions were derived in analogy to Section 2.1.1 from level 1.5 304 Å EUVI/STEREO data (using secchi_prep) and preprocessed 1.5 level 304 Å AIA/SDO data.
2.3. Error Estimation

The analysis of different parameters, for example, the Spearman correlation coefficients and fits, was done using a bootstrapping method (Efron, 1979; Efron and Tibshirani, 1993) to derive errors that take into account the sample size, outliers, and uncertainties.

3. Results

We investigated the relation between the magnetic flux density of coronal holes and the intensity distribution associated with open and closed fields around the transition region using 304 Å data and obtained the following results.

3.1. Photospheric Magnetic Field and Magnetic Elements

It was shown by Hofmeister et al. (2017) and further confirmed by Hofmeister et al. (2019) and Heinemann et al. (2019) that the signed mean magnetic field strength (consequently, open flux) of coronal holes is predominantly rooted in strong, long-living magnetic elements in the photosphere, that cover roughly 1 to 10% of the coronal hole area. Magnetic elements are either associated with the dominant polarity or the non-dominant polarity of the coronal hole. Following the work by Hofmeister et al. (2019), we first investigate the area they cover as a function of the coronal holes mean magnetic flux density. In Figure 1, we show the proportion of the coverage of non-dominant ($A^-$) to dominant polarity ($A^+$) magnetic elements as a function of magnetic field strength. We find a strong Spearman correlation of $c_{sp} = -0.84$ with a 90% confidence interval of $CI = [-0.87, -0.80]$, which shows a coverage decrease toward stronger fields (left panel). The right panel shows the area covered by supposedly open fields as a function of the magnetic flux density. We define open field as $A_{OF} = A^+ - A^-$ under the assumption that all non-dominant polarity magnetic elements close with dominant polarity magnetic elements within the coronal hole. We find a very strong, close to 1-to-1 correlation, $c_{sp} = -0.94$, $CI_{90} = [0.93, 0.96]$ between the percentage covered by open fields and the mean magnetic flux density of the coronal hole. The open field of coronal holes, estimated by the area that magnetic elements of dominant polarity cover, builds the basis for estimating the magnetic flux in coronal holes from non magnetic field data.

3.2. Coronal Holes and the Transition Region

The magnetic field in coronal holes follows a particular, but not well-known, expansion profile, where strong unipolar funnels rapidly expand into the open space before forming the approximately homogeneous vertical fields in the upper corona (Cranmer and van Ballegoijen, 2005). Closed fields of quiet coronal hole regions and small bipolar structures seem to be prevented from expanding to great heights (Wiegelmann and Solanki, 2004). To relate the magnetic field in the photosphere to the field in the transition region, we assume that in the transition region, where the 304 Å He II line is primarily formed, the space is filled with either open fields or closed fields, both anchoring in the coronal holes magnetic elements. Thereby, the closed fields are most likely associated with loops of bipolar structures, for example, magnetic elements of opposite polarity and weaker and smaller loops are supposed to close at lower heights. Figure 2 shows a coronal hole from May 29, 2013 12UT in the 193 Å and 304 Å lines. Within the small subfield, we show the LoS magnetic field whereby we
mark the dominant and non-dominant magnetic elements in blue and green. The elements are overlaid onto the 304 Å subfield image, and it is clearly apparent that the bright structures in the transition region can be associated with bipolar footpoint pairs; in contrast, the large magnetic elements of dominant polarity are not associated with any specific structure. These images are representative for the entire dataset.

Under the previously stated assumption that the space in the transition region is filled by either open, expanded fields from dominant polarity magnetic elements associated with lower 304 Å intensities or closed fields from bipolar structures that can be clearly associated with bright structures, we segment the coronal hole area as seen in 304 Å filtergrams using an intensity threshold into higher and lower intensity regions. As such, we calculate the percentage area coverage of supposedly open fields, 

$$A_{OF} = \frac{A_{THR}}{A_{CH}}$$

for a range of thresholds, whereby we define the threshold in percent of the solar disk median intensity ($I_{SD,\text{med}}$) to remove solar cycle effects, and correlate $A_{OF}$ to the signed mean magnetic flux density of the coronal hole. In addition, this analysis was also performed on quiet sun and plage subfields to determine whether these are properties unique to coronal holes. This is shown in Figure 3. The x-axis represents the upper threshold, that is, the area below the threshold is considered “open” fields, and the color shows the Spearman correlation coefficient of $A_{OF}$ to $|B_{CH}|$ for coronal holes or $A_{OF}$ to $|B_{sf}|$ for quiet Sun subfields. For coronal holes, we find a maximum in the correlation with $cc_{sp} = 0.59$, CI90 = [0.52, 0.66] at a threshold of 94% of the median solar disk (SD) intensity, whereas in quiet Sun regions, neither for actual quiet regions nor for plage regions, a clear correlation exists (nor any changes). The correlation for QS subfields does not exceed $cc_{sp} = \pm 0.25$. This suggests that the previously stated assumption of open fields is valid for coronal holes but not quiet Sun regions, which was expected. Next, we sort the coronal holes into three bins depending on their latitudinal position of their geometric center of mass (CoM; see Figure 3, bottom). From that we find a further latitudinal dependence. The strongest correlation was derived for latitudes < 20°, which already drops in the 20°–40° bin and even ceases for latitudes > 40°. Possible reasons are discussed in Section 4.

By choosing the threshold associated with the best correlation (Figure 3, top panel) we can analyze the relation in more detail. Figure 4 shows the absolute value of the signed

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**Figure 1** Left: Ratio of the area of magnetic element of non-dominant polarity to area of magnetic elements of dominant polarity in coronal holes as a function of the magnetic flux density. Right: Percentage area coverage of open magnetic elements as a function of the magnetic flux density.
Figure 2 Example of a coronal hole from May 29, 2013, 12:00UT. a) shows the coronal hole in 193 Å; b) shows the 304 Å filter, the white contour represents the coronal hole boundary as extracted by CATCH. c) shows the underlying photospheric magnetic field of a subfield as marked by the green line. d) shows the same subfield for the 304 line. Magnetic elements of dominant polarity (in this coronal hole positive) are overlayed in blue, and opposite polarity magnetic elements in green. The yellow circle mark bright structures in 304 Å that can be associated with a bipolar set of magnetic elements in the underlying photosphere. Single magnetic elements of dominant polarity are not associated with bright structures.

mean magnetic flux density ($|B_{CH}|$) of the coronal hole as a function of the area coverage of the assumed open field regions ($A_{OF}$) as extracted using the threshold of $0.94 \times I_{SD,med}$. This is done for the whole sample and three latitude bins, namely \( \text{CoM}_{LAT} \leq 20^\circ \), \( 20^\circ < \text{CoM}_{LAT} \leq 40^\circ \), and \( \text{CoM}_{LAT} > 40^\circ \). For the full sample we find a correlation of $c_{sp} = 0.59$, $\text{CI}_{90} = [0.52, 0.66]$. The different latitude bins show a latitudinal dependence of the found relation with $c_{sp} = 0.74$, $\text{CI}_{90} = [0.66, 0.81]$ in the lowest latitudinal bin which is associated with coronal holes near the solar equator. In the latitude bin covering latitudes from $20^\circ$ to $40^\circ$ a correlation of $c_{sp} = 0.50$, $\text{CI}_{90} = [0.37, 0.61]$ was found. In the highest latitude bin ($> 40^\circ$) the correlation vanishes ($c_{sp} = 0.01$, $\text{CI}_{90} = [-0.24, 0.25]$). The correlations seem to follow an exponential curve, and we use an exponential fit. For the whole dataset, the fit
Figure 3 Correlation of mean magnetic flux density ($|B_{CH}|$) of the coronal hole and the percentage area coverage ($A_{OF}$) of the coronal holes (below a set intensity threshold) as a function of the threshold normalized to the solar disk median intensity ($I_{SD}$). The bars from top to bottom are sorted according to the data (subset) used. The top bar includes all coronal holes followed by all quiet Sun areas. The next two panels show the “quiet” ($|B_{sf}| \leq 3$) and the plage ($|B_{sf}| > 3$) regions of the quiet Sun dataset. The bottom three panels show different coronal hole subsets sorted into latitude bins depending on the latitudinal position of their geometric center of mass.

\[ |B_{CH}|[G] = (0.25 \pm 0.06) \times e^{(0.032 \pm 0.003) \times A_{OF}[\%]}, \]  

and for the lowest latitude bin, a slightly steeper fit with

\[ |B_{CH}|[G] = (0.13 \pm 0.04) \times e^{(0.042 \pm 0.004) \times A_{OF}[\%]} \]

was found. With this relationship, it is possible to estimate the open flux of a coronal hole by only using two spectral filters, the 193 Å filter to define the coronal hole boundary and the 304 Å filter to derive the open flux regions. Further, we estimate the uncertainty in the fit to be between 40% for low open magnetic field areas and 60% for higher ones (see Figure 4, shaded area). The uncertainties were estimated by bootstrapping the fit over the sample with the uncertainties in B (from CATCH) in mind (see Section 2.3). Due to the exponential nature, that is, saturating behavior toward 100% coverage, the uncertainty increases toward higher field strengths/higher coverage.

### 3.3. Far-Side Coronal Holes

In Section 3.2, we have established a relationship between the open magnetic field and the transition region intensity distribution in coronal holes. Using this relation, we can estimate the open flux based on 304 Å observations. Using the different perspectives from STEREO satellites allows us to derive the magnetic flux of coronal holes from EUV observations at
Figure 4  Coronal hole mean magnetic flux density (|B_{CH}|) as function of the percentage area coverage (A_{OF}) of assumed open fields extracted using an upper threshold of 0.94 × I_{SD,med}. Panels a) through d) show all coronal holes and three subsets sorted by their latitudinal position. The red lines show an exponential fit to the data, and the shaded areas give the fit uncertainties.

viewpoints not visible from Earth. Between 2012 and 2017, both STEREOs were separated by at least 110° from Earth, effectively imaging the far-side of the Sun. As there is no remote sensing magnetic field instrument on either STEREO, this relation might be used to estimate the far-side open flux during that time. To be able to use this relation, a calibration from SDO to STEREO has to be established. For this, 13 coronal holes of medium to large area were chosen, which were observed by both STEREOs and SDO with low longitudinal separation. The low separation angle between the spacecraft allows the approximation of a similar magnetic flux density. As the magnetic field evolution of a coronal hole is not dependent on the coronal holes area or lifetime evolution, the statistical uncertainty may be even lower. Even though SDO and STEREO observe the same waveband (304 Å), the instruments (e.g., filter, mirror, ccd, age) are not identical. The AIA/SDO EUV filters are built with a spectral Full Width Half Maximum (FWHM) of ≈ 1 nm (Boerner et al., 2014), whereas the 304 Å EUVI/STEREO filter has an FWHM of 3 nm (Howard et al., 2008). These differences make an intercalibration necessary. For this, we use a simple approach
assuming that the relation found for SDO data is also valid for STEREO data. However, the threshold for the detection of the supposedly open fields might not be the same. Thus we calculated the root mean square error (RMSE) between the area coverage of STEREO and SDO in 304 Å while varying the extraction threshold for STEREO and keeping the SDO threshold fixed at 0.94 \times I_{SD,med} for SDO (left panel of Figure 5). From this we derive a minimum at 0.78 \times I_{SD,med} for both STEREOs. We find that this threshold calibration yields similar percentage area ratios in 304 Å (A_{OF}) between the respective SDO and STEREO coronal holes (indicated by the black line connecting red, black, and blue points in the right panel of Figure 5. For the thresholds 0.94 and 0.78 \times I_{SD,med} for SDO and STEREO, respectively, we find a mean error (ME) of ME_{STA} = -0.7 \% A_{OF} and ME_{STB} = -0.2 \% A_{OF}, that is, the relative difference is < 1\%. The RMSE was found to be RMSE_{sta} = 5.0 \% A_{OF} and RMSE_{STB} = 6.8 \% A_{OF}, or a relative absolute difference of 6.6\% and 9.0\%, respectively. To verify that the data from STEREO also follow the same relation as found from SDO data, we show on the right of Figure 5 the signed mean magnetic flux density (|B_{CH}|) as a function of the area coverage (A_{OF}) for all three spacecrafts. A single coronal hole is shown connected by a black line. We find that the extracted areas ratios for STEREO match the SDO area ratios very well and lie within the uncertainty range of the fit derived in Section 3.2 (see Equation 1). However, we do note that to independently fit the data obtained from STEREO observations or undoubtedly prove the relation for STEREO, the sample is too small and temporally too constrained. However, validity of the relation is suggested by the results.

The found results allow an estimation of the non-polar far-side open magnetic flux by first extraction coronal holes using, for example, the 195 Å filter and then determining the percentage of the area below a threshold of 0.78 \times I_{SD,med} (0.94 \times I_{SD,med} for SDO) in 304 Å STEREO observations. This gives an estimate of the signed mean magnetic flux density including the uncertainties. From the coronal hole area and signed mean magnetic
flux density the open flux for each coronal hole can be determined and subsequently the open far-side flux can be estimated.

4. Discussion

The difference between open flux observed remotely and measured in situ is above a factor of 2 (Linker et al., 2017; Lowder, Qiu, and Leamon, 2017; Wallace et al., 2019), which might partly be due to the uncertainty in estimating the far-side open flux from indirect methods like synoptic charts or flux-transport models. This new method to estimate the open flux from far-side remote sensing observations may allow closing the gap of the “open flux problem” and help in validating new methods to estimate the far-side magnetic fields. With the methodology reported in this study, it is possible to derive the far-side open flux with an uncertainty between 40% and 60% (depending on the coverage) from the uncertainty in the magnetic flux density, which is close to the uncertainty in the open field of a single coronal hole observed at the near-side of 45%, as reported by Linker et al. (2021). However, the value obtained by Linker et al. (2021) includes an estimate for the uncertainty in the coronal hole area (∼26%), which was not considered in this study.

In the photosphere, we find a linear relation between the area covered by the magnetic elements and the mean magnetic flux density of the coronal hole, but in the chromosphere/transition region, we choose to use an exponential fit. In the photosphere the area of a magnetic element is determined entirely by its flux, or vice versa (see Hofmeister et al., 2019). In the transition region, we believe that the area covered by fields extending from those photospheric magnetic elements is determined primarily from the magnetic pressure balance between open and closed fields. The interaction of loops from bipolar structures and open fields from unipolar funnels will determine the area ratio related to open fields (see the theoretical concepts by Cranmer and van Ballegooijen, 2005; Wedemeyer-Böhm, Lagg, and Nordlund, 2009). It seems from Figure 4 that this relation can be described by an exponential function rather than by a linear one as found in the photosphere.

We find that the relation between the area coverage and the magnetic field starts to decrease towards higher latitudes, which we strongly assume to be a projection effect rather than an actual physical effect. The AIA EUV filters cover emission from multiple atmospheric heights. Due to this, in combination with the view angle, the same structure might show different signatures depending on what direction and angle they are observed from. In the case of coronal holes, we suppose that the area of bright structures depends on these, however, in a nonlinear way. We tried to correct for the latitudinal dependence (not shown in the paper) and found no correlation between extracted areas and latitudes of these bright structures. This leads to the assumption that also the orientation plays a role in how big the structure is when seen at different angles (Feng et al., 2007; Aschwanden et al., 2008). By understanding the projection effects and finding a way to correct for it, it might be possible to significantly increase the correlations and thus lowering the uncertainties. Further, the increasing uncertainty in magnetic field observation due to the LoS angle (Petrie and Haislmaier, 2013; Petrie, 2015) and due to the zero point uncertainty (Li, Feng, and Wei, 2021) might contribute to the decrease of the correlation. Future data from missions, which will go out of the ecliptic (e.g., Solar Orbiter, Solaris), will help to further constrain the uncertainties.

Except of the data uncertainties, we also have to discuss the assumptions and simplifications we have made. Firstly, we assumed that the field in the upper chromosphere/transition region is mostly filled by magnetic fields that eventually are considered open, or high loops
rooted in magnetic elements. Although this was done in accordance with the models and ideas of the coronal structure as proposed by Cranmer and van Ballegooijen (2005) and Wedemeyer-Böhm, Lagg, and Nordlund (2009), it has not yet been conclusively shown if that is the case. Secondly, it was assumed that the relation between the coronal hole signed mean magnetic flux density and the area coverage is similar for SDO and STEREO. Although the 13 coronal holes are a subset of the full SDO sample and follow the correlation, it is not possible to derive the relation from this data alone for the STEREOs. This is due to the small sample of usable data, as there is only a short time window where both SDO and STEREO were observing at a low longitudinal separation. By increasing the dataset to include coronal holes at larger longitudinal separation angles of the spacecraft, we would also increase the uncertainty in the magnetic field values and area differences due to the coronal holes evolution to the point where a meaningful correlation can no longer be derived.

5. Summary and Conclusions

In this study, we present a new method to estimate the far-side open flux from STEREO observations. We correlate magnetic field structures within coronal holes from the photosphere to the transition region and derive an estimation of the open flux from 304 Å images. We calculate an interinstrument calibration to allow the use of this method for STEREO coronal holes. Our study can be summarized as follows.

i) We showed that the intensity distribution and, as such, the correlation of dark regions in 304 Å to the magnetic flux density in coronal holes significantly differ in quiet Sun and plage regions.

ii) We showed that the area coverage of photospheric magnetic elements of coronal holes can be approximated in 304 Å by the area proportion below a threshold of 78% (STEREO) or 94% (SDO) of the solar disk median intensity.

iii) We successfully calibrated the area ratios for SDO and STEREO (RMSE < 10%$A_{OF}$; ME < 1%$A_{OF}$). This allows the use of the found relation on STEREO data.

iv) From the relation between the area coverage ($A_{OF}$) in 304 Å and signed mean magnetic flux density ($|B_{CH}|$), we derived that the open flux of a coronal hole can be approximated as

$$\Phi_{CH}|[Mx] = (0.25 \pm 0.06) \times A_{CH} \times e^{(0.032 \pm 0.003) \times A_{OF}[^\%]}.$$  

(3)

This new method on how to estimate the far-side flux may help in deriving far-side fluxes from helioseismic data or tune flux transport models. It can help to improve the estimates of global open magnetic flux needed for space weather forecasting and as input for heliospheric MHD simulations (e.g., Pomoell and Poedts, 2018). Finally, the additional information that can be obtained using this method can act as input for L5 prestudies (e.g., in preparation of Lagrange L5 mission planned by ESA).

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Declarations

Disclosure of Potential Conflicts of Interest  The authors declare that they have no conflicts of interest.

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