On the signature of $z \sim 0.6$ superclusters and voids in the Integrated Sachs-Wolfe effect

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\textbf{ABSTRACT}

Through a large ensemble of Gaussian realisations and a suite of large-volume $N$-body simulations, we show that in a standard ΛCDM scenario, supervoids and superclusters in the redshift range $z \in [0.4, 0.7]$ should leave a small signature on the Integrated Sachs Wolfe (ISW) effect of the order $\sim 2 \mu K$. We perform aperture photometry on WMAP data, centred on such superstructures identified from SDSS LRG data, and find amplitudes at the level of $8 – 11 \mu K$ – thus confirming the earlier work of Granett et al. (2008b). If we focus on apertures of the size $\sim 3.6^\circ$, then our realisations indicate that ΛCDM is discrepant at the level of $\sim 4 \sigma$. However, if we combine all aperture scales considered, ranging from $1^\circ–20^\circ$, then the discrepancy becomes $\sim 2 \sigma$, and it further lowers to $\sim 0.6 \sigma$ if only 30 superstructures are considered in the analysis (being compatible with no ISW signatures at 1.3σ in this case). Full-sky ISW maps generated from our $N$-body simulations show that this discrepancy cannot be alleviated by appealing to Rees-Sciama (RS) mechanisms, since their impact on the scales probed by our filters is negligible. We perform a series of tests on the WMAP data for systematics. We check for foreground contaminants and show that the signal does not display the correct dependence on the aperture size expected for a residual foreground tracing the density field. The signal also proves robust against rotation tests of the CMB maps, and seems to be spatially associated to the angular positions of the supervoids and superclusters. We explore whether the signal can be explained by the presence of primordial non-Gaussianities of the local type. We show that for models with $f_{NL}^{\text{local}} = \pm 100$, whilst there is a change in the pattern of temperature anisotropies, all amplitude shifts are well below $<1 \mu K$. If primordial non-Gaussianity were to explain the result, then $f_{NL}^{\text{local}}$ would need to be several times larger than currently permitted by WMAP constraints.

\textbf{Key words:} cosmology: observations – cosmic microwave background – large-scale structure of the Universe – galaxies: clusters: general

1 INTRODUCTION

Over the last fifteen years, evidence has been mounting from various cosmological probes to support the case for an accelerating universe. It can be argued that the first compelling evidence for this arose from the study of the light curves of distant type Ia supernovae \cite{Riess98, Perlmutter99}. Currently, the strongest support for this picture comes from the combination of observations of the Cosmic Microwave Background radiation (hereafter CMB), and from measurements of the clustering of galaxies. From the CMB side, the Wilkinson Microwave Anisotropy Probe (hereafter, WMAP) experiment \cite{Spergel03, 2007ApJS..170..377S, Komatsu11} provided a precise measurement of the angular size of the sound horizon at recombination, which supported the case for a spatially flat universe. On the clustering side, data from surveys like the 2-degree Field Redshift Survey \cite{Cole01} and the Sloan Digital Sky Survey (hereafter SDSS) \cite{Tegmark06} required the density in matter to be sub-critical, hence leading to the inference that $\sim 70$ per cent of the current energy density of the Universe is in a form of energy that behaves like a cosmological constant, and so acts as a repulsive gravitational force. The energy density driving the accelerated

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expansion is unknown and so has been dubbed Dark Energy (hereafter DE). Uncovering the true physical nature of the DE is one of the main targets for many ongoing and upcoming surveys of the Universe.

Standard linear cosmological theory states that if the Universe undergoes a late-time phase of accelerated expansion, then gravitational potential wells on very large scales ($\gtrsim 100\,h^{-1}\text{Mpc}$) will decay. This evolution of the potential wells introduces a gravitational blueshift in the photons of the CMB that is known as the Integrated Sachs-Wolfe effect (ISW). This effect constitutes an alternative window to DE, and can be directly measured by cross-correlating CMB maps with a set of tracers for the density field, which sources the potentials (Crittenden & Turok 1996). As soon as the first data sets from WMAP were released, several works claimed detections of the ISW at various levels of significance (Scranton et al. 2003; Fosalba et al. 2003; Boughn & Crittenden 2004; Fosalba & Gaztanaga 2004; Nolta et al. 2004; Ashordi et al. 2004; Padmanabhan et al. 2004; Cabré et al. 2006; Giannantonio et al. 2006; Vielva et al. 2006; McEwen et al. 2007). Subsequent analysis has led some researchers to be more cautious about interpreting these early detections (Hernández-Monteagudo et al. 2006; Rassat et al. 2007; Belby et al. 2010; López-Corredoira et al. 2011; Hernández-Monteagudo et al. 2010; Frances & Peacock 2010).

As emphasized by Hernández-Monteagudo (2008), the true ISW effect should only be detectable for deep galaxy surveys that cover a substantial fraction of the sky. However, an erroneous interpretation of ISW cross correlation studies may be obtained from systematic errors, such as residual point source emission in CMB maps or presence of spurious galaxy auto-power on large angular scales (see also Hernández-Monteagudo 2010, for details on the WMAP – NVSS cross-correlation analysis). In particular, the issue of excess power on large scales has been noted in several works (Ho et al. 2008; Hernández-Monteagudo 2010; Thomas et al. 2011; Giannantonio et al. 2012), but it is not yet fully accounted for.

Amongst the subsequent ISW cross-correlation studies in the literature, there is the particularly puzzling work of Granett et al. (2008), hereafter G08. Their analysis yielded one of the highest detection significances in the literature. G08 implemented the following novel approach: they produced a catalogue of superclusters and supervoids from SDSS data, and stacked WMAP-filtered data on the positions of these structures with apertures of the order $\sim 4\,\circ$. They obtained a $\sim 4\sigma$ ISW detection. Unlike previous works on the subject, the analysis focused on a particular subset of the available large-scale structure (hereafter LSS) data. Subsequent studies have investigated the origin of the signal and assessed its compatibility with the ΛCDM scenario. (Pápai & Szapudi 2010; Pápai et al. 2011; Nadathur et al. 2012). While some works found the G08 results compatible, others found the measured amplitudes too high to be consistent (Granett et al. 2008; Nadathur et al. 2012; Fender et al. 2012; Inoue et al. 2012; Inoue et al. 2013). Currently, the G08 results remain unexplained.

In this work we shall attempt to shed new light on this problem. The paper breaks down as follows: In §2 we give a brief theoretical overview of the ISW effect, underlining the expectation for the ISW signal from a cross-correlation analysis of the data used in G08. In §3 we perform a cross-check of the G08 results. In §4 we test whether the G08 results are consistent with expectations for the ΛCDM model. This is achieved by using a large ensemble of Gaussian Monte-Carlo realisations. We also generate full-sky nonlinear ISW maps by ray-tracing through a suite of N-body simulations. In §5 we determine the level of significance at which the results disagree with the ΛCDM paradigm. We explore systematic errors in the foreground subtraction for WMAP. We also investigate whether the excess signal is consistent with primordial non-Gaussianities of the local type. Finally, in §6 we summarise our findings and conclude. While this paper was in the process of submission, a parallel work on this subject from Fender et al. (2012) appeared in the internet.

This work is reaching to similar conclusions to ours in some of the issues addressed in this work.

Unless stated otherwise, we employ a reference cosmological model consistent with WMAP7 (Komatsu et al. 2011): the energy-density parameters for baryons, CDM and cosmological constant are $\Omega_b = 0.0456$, $\Omega_cdm = 0.227$, $\Omega_{\Lambda} = 0.7274$; the reduced Hubble rate is $h = 0.704$; the scalar spectral index is $n_s = 0.963$; the rms of relative matter fluctuations in spheres of $8\,h^{-1}\text{Mpc}$ radius is $\sigma_8 = 0.809$, and the optical depth to last scattering is $\tau = 0.087$.

2 THEORETICAL PERSPECTIVE

2.1 The ISW effect

Observed CMB photons are imprinted with two sets of fluctuations: primary anisotropies, sourced by fluctuations at the last-scattering surface, and secondary anisotropies, induced as the photon propagates through the late-time clumpy Universe. The physics of the primary anisotropies is well understood (Dodelson 2003; Weinberg 2008). There are a number of physical mechanisms that give rise to the generation of secondary anisotropies (for a review see The Planck Collaboration 2006) and one of these is the red-shifting of the photons as they pass through evolving gravitational potentials. The linear version of this effect is termed the Integrated Sachs-Wolfe effect (Sachs & Wolfe 1967) and its nonlinear counter-part is termed the Rees-Sciama effect (Rees & Sciama 1968).

The observed temperature fluctuation induced by gravitational redshifting may be written as (Sachs & Wolfe 1967):

$$\frac{\Delta T(\hat{n})}{T_0} = -\frac{2}{c} \int_{t_{10}}^{t_0} dt \dot{\Phi}(\hat{n}, \chi),$$

where $\hat{n}$ is a unit direction vector on the sphere, $\Phi$ is the dimensionless metric perturbation in the Newtonian gauge, which reduces to the usual gravitational potential on small scales, the 'over dot' denotes a partial derivative with respect to the coordinate time $t$ from the FLRW metric, $\chi$ is the comoving radial geodesic distance $\chi = \int dt/a(t)$, and $a(t)$ is the speed of light and $a(t)$ is the dimensionless scale factor.

On scales smaller than the horizon, relevant to our simulation boxes, the perturbed Einstein equations in Newtonian gauge lead to a perturbed Poisson equation. This enables us
to relate potential and matter fluctuations [Dodelson 2003]:

\[ \nabla^2 \Phi(x; t) = 4\pi G \bar{\rho}(t) \delta(x; t) a^2(t), \]

where \( \bar{\rho}(t) \) is the mean matter density in the Universe and the density fluctuation is defined \( \delta(x; t) \equiv [\rho(x, t) - \bar{\rho}(t)]/\bar{\rho}(t) \). This equation may most easily be solved in Fourier space:

\[ \Phi(k; t) = -4\pi G \bar{\rho}(t) a^2(t) \frac{\delta(k; t)}{k^2}. \]

Differentiation of the above expression gives

\[ \dot{\Phi}(k; t) = \frac{3}{2} \Omega_m H_0^2 k^{-2} \left[ \frac{H(t)}{a(t)} \delta(k; t) - \frac{\dot{\delta}(k; t)}{a(t)} \right], \]

where we used the fact that \( [a^2(t) \bar{\rho}(t)] \) is a time-independent quantity in the matter-dominated epoch and \( \Omega_m \equiv \Omega_{\text{dm}} + \Omega_b \). In the above, we also defined \( H(t) \equiv \dot{a}(t)/a(t) \) and \( \Omega_m(t) \equiv \bar{\rho}(t)/\rho_{\text{crit}}(t) \), with \( \rho_{\text{crit}}(t) = 3H^2(t)/8\pi G \). All quantities with a subscript 0 are to be evaluated at the present epoch. In the linear regime, density perturbations scale as \( \delta(k, a) = D(a) \delta(k, a_0) \). Inserting this relation into Eq. (4) gives,

\[ \dot{\Phi}(k; t) = \frac{3}{2} \Omega_m H_0^2 k^{-2} \frac{H(t)}{a(t)} \left[ 1 - \frac{d \log D}{d \log a} \right] \delta(k; a_0). \]

In the matter-dominated phase, the Universe expands as in the Einstein-de Sitter case and consequently density perturbations scale as \( D(a) \propto a \). Thus, for most of the evolution of the late-time Universe the bracket, \( [1 - d \log D / d \log a] \), is close to zero. In the ΛCDM model it is only at relatively late times that this term is non-zero.

Alternatively, in the nonlinear regime \( \delta(k, a) \neq D(a) \delta(k, a_0) \), and this gives rise to additional sources for the heating and cooling of photons [Smith et al. 2009, Cai et al. 2002, 2010].

2.2 Expectations for cross-correlation analysis

The expected signal for the ISW-density tracer cross-correlation analysis has been described by several authors (Crittenden & Turok 1996; Hernández-Monteagudo 2008; Smith et al. 2009) and we here simply quote the main results. For a survey of galaxies (or more generically, objects that are biased density tracers) the ISW-density angular power spectrum can be written:

\[ C^\text{ISW}_\ell \equiv \left( \frac{2}{\pi} \right) \int_0^\infty k^2 dk P_m(k) \]

\[ \times \int_0^\infty d\chi \, j_l(k\chi) \chi^2 W_1(\chi) n_e(\chi) b(\chi, k) D(\chi) \]

\[ \times \int_0^\infty d\chi \, j_l(k\chi) \left[ \frac{-3\Omega_m H_0^2}{k^2} \frac{d(D(\chi)/a(\chi))}{d\chi} \right] / \chi^3, \]

where \( P_m(k) \) denotes the linear matter power spectrum at the present time, the super-script \( g \) refers to the objects (galaxies in most cases, but in ours it will refer to voids or superclusters) probing the gravitational potential wells. In the above \( n_e(\chi) \) denotes the average comoving object number density; \( W_1(\chi) \) denotes the instrumental window function providing the sensitivity of the instrument to the objects at distance \( \chi \); the \( j_l(x) \) are the usual spherical Bessel functions of order \( l \); and \( b(\chi, k) \) denotes the bias of the tracer population with respect to the matter density field. This last factor may be both a function of time \( \chi \) and scale \( k \) [Smith et al. 2007], but for simplicity we shall simply assume that the bias equals unity for the objects in our catalogue.

In this measurement the primary CMB signal acts as noise. If we take this into account and also the variance due to the density field, then the \( S/N \) with which we expect to detect the cross-correlation for a given multipole is (e.g., Crittenden & Turok 1996):

\[ \left( \frac{S}{N} \right)_\ell = \frac{C^\text{ISW}_\ell}{C^\text{CMB}_\ell (C^\text{ISW}_\ell + 1/\bar{n}_g)} + \left( C^\text{ISW}_\ell \right)^2, \]

where \( C^\text{CMB}_\ell \) and \( C^\text{ISW}_\ell \) represent the auto power spectra of the temperature fluctuations and the density tracers; \( \bar{n}_g \) denotes the average angular object number density and hence the term \( 1/\bar{n}_g \) denotes the shot-noise. In our forecast we shall neglect this term (hence the predicted significance will be slightly over optimistic). The factor \( f_{\text{sky}} \) refers to the fraction of the sky jointly covered by both the CMB and the object surveys. The cumulative \( S/N \) for all harmonics smaller than \( \ell \) can then be written:

\[ \frac{S}{N}(< \ell) = \sum_{\ell'=2}^\ell \left( \frac{S}{N} \right)_{\ell'}, \]

where the monopole and dipole have not been included.

2.3 Expectations for ISW from data used in Granett et al.

We now turn to the question of what \( S/N \) should G08 have expected to find in their data. G08 used a sample of 1.1 million Luminous Red Galaxies (hereafter LRG) selected from the SDSS data release 6 (hereafter DR6) [Adelman-McCarthy et al. 2006]. This sample covered roughly 7500 square degrees and spanned a redshift range of \( 0.4 < z < 0.75 \). From this sample they identified regions as supervoids or superclusters using the algorithms ZOBov and VBOBZ respectively, [Neyrinck 2008, Neyrinck et al. 2004]. The significance of these regions was chosen to be at least at the 2σ-level relative to a Poisson sample of points. G08 selected the largest 50 superclusters and supervoids for their analysis. Their catalogue is publicly available.

In the left panel of Fig. 1 the dot-dashed and dotted histograms denote the redshift distributions of supervoids and superclusters, respectively. The thick solid line represents an analytic fit that we have constructed, which attempts to be a compromise between the two. Our fitting function extends to slightly lower redshifts than the G08 catalogue, and this will translate into a slightly higher ISW prediction.

The middle panel of Fig. 1 presents the angular cross-correlation of voids versus superclusters. We may have overlooked b = 1 for both voids and clusters. In reality the void/cluster regions will be anti-biased/biased and so the two signals will differ. However, since here we are more concerned with the \( S/N \) this simplification does not matter.

\[ \text{http://skysrv.pha.jhu.edu/~neyrinck/vbobz/} \]

\[ \text{http://ifa.hawaii.edu/cosmowave/supervoids/} \]
especially since we are neglecting the effects of shot-noise on the cross-spectra. We also point out that our predictions for the ISW-induced cross correlation signal of superclusters and supervoids in the SDSS sample are quite similar to the predictions for the cross-correlation of AGNs \((z < 2)\) in the NVSS catalogue (after adopting the model of Ho et al. 2008, see the dashed line in the middle panel of Fig. 1).

The right panel of Fig. 1 presents the predictions for the cumulative \(S/N\) for the SDSS supercluster and supervoid analysis. These predictions (solid black line) show that, for a \(\Lambda\)CDM model, one should expect no more than \(\approx 1.3\) \(\sigma\) significance. In contrast, the prediction for NVSS (dashed line) is close to \(\approx 5.5\) (obtained after also neglecting shot noise). This is not surprising, since the G08 supervoid and supercluster catalogue is relatively shallow, spanning the redshift range \((0.74 < z < 0.7)\), and covers only a modest fraction of the sky \((f_{\text{sky}} \approx 0.18)\). The NVSS is instead significantly deeper and wider. We hence conclude that had G08 applied a standard ISW cross-correlation analysis to their data, then in the framework of the \(\Lambda\)CDM model, there would have been very little chance for detecting any genuine signal at high significance.

3 CROSS-CHECKING GRANETT ET AL.

3.1 CMB data

The WMAP experiment scanned the CMB sky from 2001 until 2010 in five different frequencies, ranging from 23 GHz up to 94 GHz. The angular resolution in each band improves with the frequency, but it remains better than one degree in all bands. The \(S/N\) is greater than one for multipoles \(\ell < 919\) (Jarosik et al. 2010), and in particular, on the large scales of interest for ISW studies, the galactic and extragalactic foreground residuals are below the \(15\mu\text{K}\) level outside the masked regions (Gold et al. 2011).

We concentrate our analysis on the foreground-cleaned maps corresponding to bands Q (41GHz), V (61GHz) and W (94GHz), after applying the conservative foreground mask KQ75y7, which excludes \(~25%\) of the sky. At the scales of interest, instrumental noise lies well below cosmic variance and foreground residuals, and hence will not be considered any further. The ISW is a thermal signal whose signature should not depend upon frequency and hence should remain constant in the three frequency channels. All of the WMAP data employed in this analysis were downloaded from the LAMBDA site\(^4\).

3.2 Supercluster and Supervoid data

For our tracers of the LSS, we use the same supercluster and supervoid catalogue as used by G08. As described earlier, the catalogue was constructed after applying the ZOBOV and VOBOZ algorithms to search for supervoids and superclusters in the LRG sample extracted from SDSS DR6, respectively. G08 used the 50 largest supervoids and superclusters. They claimed that this cut yielded the highest statistical significance, in that it minimized the contamination from spurious objects, whilst at the same time it provided sufficient sampling to beat down the intrinsic CMB noise.

3.3 Methodology

In their approach G08 have applied a top-hat compensated filter or Aperture Photometry (AP) method to the CMB map(s) positions of voids and superclusters. This filter subtracts the average temperature inside a ring from the average temperature within the circle limited by the inner radius of the ring. In order to have equal areas in both cases, the choice of the outer radius of the ring is \(\sqrt{2}R\), with \(R\) the inner radius of the ring. In this way, fluctuations of typical

\(^4\) http://lambda.gsfc.nasa.gov

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size $R$ are enhanced against fluctuations at scales smaller or larger than such radius. Although G08 present results for apertures ranging from $3^\circ$ up to $5^\circ$, most of the conclusions are driven from the $R = 4^\circ$ choice, for which highest statistical significance is achieved: they find that AP stacks on the position of voids (superclusters) yield a decrement (increment) of $\sim -11.3 \mu K$ ($7.9 \mu K$) at $3.7$ ($2.6$) $\sigma$ significance level. However, it turns out that, according to G08, the typical size of clusters and voids are $\sim 0.5^\circ$ and $2^\circ$, respectively, which seem to lie at odds with the aperture choice of $4^\circ$. Potentials are known to extend to larger scales than densities, and it is a priori unclear which aperture radius should be used. This fact motivates a systematic study in a relatively wide range of aperture radii.

3.4 Stacking analysis on real data

We apply the G08 method on the Q, V, and W bands of the WMAP data using the SDSS supercluster and supervoid catalogue. We have considered AP filters in 15 logarithmically spaced bins in the angular range $1^\circ - 20^\circ$. The filters were placed on the centers of the objects, as they are provided by the catalogue.

Figure 2 displays the results for the stacked signal as a function of the AP filter aperture size in degrees. The red, green and blue symbols refer to results from the Q, V and W bands, respectively. We clearly see that there is practically no frequency dependence. The error bars are computed after repeating the analysis on 30 random sets of 50 objects placed in the un-masked region of the sky. Our findings are in good agreement with those of G08: voids and supercluster regions yield a slightly asymmetric pattern, with voids rendering amplitudes of $\sim -11 \mu K$ for apertures of $\sim 3.6^\circ$, and superclusters giving rise to increments of $\sim 9 \mu K$ at that same scale. In these two cases, the significance is about $-3.3 \sigma$ and $2.3 \sigma$, which on combination yields a combined significance $\sim 4 \sigma$. Again, this is in good agreement with G08. Furthermore, the scale showing highest $S/N$ is $\lesssim 4^\circ$, as the significance rapidly drops for smaller and larger apertures. Intuitively, this seems to be in contradiction with the idea of ISW fluctuations being large-scale anisotropies, since in such case one would expect to attain high $S/N$ also for moderately large ($\gtrsim 5^\circ - 10^\circ$) apertures.

4 ARE THE RESULTS CONSISTENT WITH THE VANILLA $\Lambda$CDM UNIVERSE?

4.1 Gaussian realisations

What is not clear from the analysis of the previous section, is whether the $\sim 4\sigma$ detection from the stacked supercluster/supervoid regions is consistent with what one expects from the standard $\Lambda$CDM model (Komatsu et al. 2011). We now attempt to understand the dependence of the expected signal and its errors on the filter size. To that end, we repeat the above analysis on a set of Gaussian realisations of both the LSS distribution and the corresponding CMB temperature anisotropy distribution which would result in our $\Lambda$CDM model.

The CMB maps are constructed in a two-step process: first, we generate a Gaussian map of projected density, following the angular power spectrum built upon the redshift window function $W_g(r)$ displayed in the left panel of Fig. 1. This density map is used for (i) constructing a supercluster and supervoid catalogue (see below), and (ii) generating an ISW component. This ISW component is correlated to the density map as predicted by Eq. 6 (see, e.g., Cabré et al.)
Figure 4. Top panel: Full-sky, nonlinear ISW map arising from structures between $z = 0.0$ and $z = 1.0$, estimated from one of the zHORIZON simulations. The sky map was pixelated using the HEALPix package with a resolution of $N_{\text{side}} = 256$, which corresponds to 786,432 pixels. Bottom panel: full-sky projected over-density map for the distribution of cold dark matter structures located in the redshift shell $z = [0.260, 0.366]$ for the same $N$-body simulation. The map was pixelated at the same resolution as the ISW map and smoothed with a Gaussian filter of scale FWHM = 16.9 arcmins (roughly the angular size subtended by $1 \ h^{-1}\text{Mpc}$ at $z = 0.3$). In both panels the graticule scale indicates $30^\circ$ divisions.

Second, we generate the primary anisotropy signal at $z \approx 1050$. This is taken to be completely uncorrelated with respect to the projected density map. This is not exactly true due to the lensing of the CMB, but it is still a very good approximation on the large angular scales of interest in this study. The simulated ISW map is then directly co-added to the primary CMB temperature map. We have checked that the cross-correlations of the simulated density and CMB maps are in direct agreement with a numerical evaluation of Eq. (6).

All of the simulated sky maps were generated using the equal area pixelization strategy provided by HEALPix\(^5\) (Górski et al. 2003). We take the pixel scale to be $\approx 15'$, corresponding to a HEALPix resolution parameter of $N_{\text{side}} = 256$. For each simulated LSS map we smooth the map with a Gaussian aperture of FWHM=2$, and identify those peaks and troughs which exceed a given threshold $\nu|\sigma|$ as being associated with supervoids and superclusters, where $\sigma$ in this context refers to the density field rms. The threshold $\nu$ is chosen to have an object density similar to that of superclusters and voids in the real catalogue under the SDSS

\(^5\) URL site: http://healpix.jpl.nasa.gov
footprint. Note that this Gaussian smoothing takes place only at the step of ‘identifying’ superstructures in the density maps. To check the dependence on the threshold choice, we bracket the preferred value of $\nu$ with two other values, one above and one below it. The final choice for the $\nu$ value set was 2.5, 2.8 and 3.2.

To each simulated CMB sky, we also add a noise realization following the anisotropic noise model provided in the LAMBDa site. We then exclude pixels in accordance with the intersection of the WMAP KQ75y7 sky mask and the SDSS DR6 data footprint.

Figure 3 presents the ensemble-averaged results obtained from 5000 Gaussian Monte-Carlo realisations. As expected, for the three adopted thresholds, overdensities (or positive excursions in the projected density map) yield a positive signal for the stacked aperture analysis (as displayed by the squares in the plots), whereas underdensities yield negative ones (circles in the plot). The Monte-Carlo realisations also enable us to compute the variance on the measurements. On taking the ratio of the mean signal and the rms noise, we obtain direct estimates of the $S/N$ for each given aperture bin. The coloured solid lines in the plot present our direct measurements of the $S/N$. Thus we clearly see that the scatter induced by the CMB generated at $z \approx 1050$ is the dominant source of noise, keeping the $S/N$ for each angular bin below unity.

For lower thresholds there is more area covered and intuitively one would expect a higher $S/N$, as it seems to be the case. Our realisations also provide higher ISW amplitudes for higher thresholds, and this makes sense since deeper voids/potential wells should have a stronger impact on CMB photons. Nevertheless, in all cases typical amplitudes remain at the level of 1–2 $\mu$K. The aperture at which the AP outputs provide the highest amplitude does not show any strong dependence upon the threshold $\nu$, and seems to lie in a wide angle range within $[3^\circ, 8^\circ]$. For apertures larger than $10^\circ$, the $S/N$ for the lowest threshold starts dropping slowly, and becomes half of its maximum value at an aperture of $20^\circ$. For higher thresholds this decrease is found to be even shallower.

4.2 Generation of nonlinear ISW and density maps from $N$-body simulations

The previous subsection has shown that the Gaussian realisations of the $\Lambda$CDM universe are in tension with the excess signal found by G08. One weak point in the above analysis is that the density and late-time potential field are not necessarily well described by a Gaussian process, since nonlinear evolution under gravity drives the initially Gaussian distribution of density fluctuations towards one that is non-Gaussian at late times. In order to test whether nonlinear evolution could explain the excess signal seen by G08, we now turn to the challenge of constructing fully nonlinear maps of the density field and ISW effect from $N$-body simulations.

The 8 simulations that we employ for this task are a sub-set of the zHORIZON simulations. These simulations were used in Smith et al. (2009) to calculate the expected ISW-cluster cross-power spectra. In brief, each simulation follows the gravitational evolution of $N = 750^3$ dark matter particles in a box of comoving size $L = 1500 h^{-1}$ Mpc.

The cosmological model employed was a flat $\Lambda$CDM model: $\Omega_{m,0} = 0.25$; $\sigma_8 = 0.8$; $n_s = 1.0$; $h = 0.72$, $\Omega_{b,0} = 0.04$. The transfer function for the simulations was generated using the cmbfast code (Seljak & Zaldarriaga, 1996). The initial conditions were laid down at redshift $z = 49$ using the code 2LPT (Scoccimarro, 1998; Crocce et al. 2006). Each initial condition was integrated forward using the publicly available cosmological $N$-body code Gadget-2 (Springel, 2005). Snapshots of the phase space were captured at 11 logarithmically-spaced intervals between $a = 0.5$ and $a = 1.0$.

In order to generate full-sky nonlinear ISW maps we roughly follow the strategy described in Cai et al. (2010), but with some minor changes. Full details of how we construct our maps can be found in Appendix A. In summary, we used the density and divergence of momentum fields to solve for $\Phi$ for each snapshot. We then constructed a backward light-cone from $z = 0.0$ to $z = 1.0$ for $\Phi$. We then pixelated the sphere using the HEALPix equal-area decomposition, taking the pixel resolution to be $N_{\text{side}} = 256$, which corresponds to 786,432 pixels on the sphere.

For each pixel location, we then fired a ray through the past light-cone of $\Phi$ and accumulated the line-of-sight integral given by Eq. (1). Note that we only consider the ISW signal coming from $z < 1$, since we do not expect a significant cross-correlation between the relatively low-redshift density slices for SDSS and the ISW from $z > 1$. The top panel of Fig. 4 shows one of the ISW maps that we have generated from the zHORIZON simulations.

We next generated the projected density maps. These were done by first constructing the projected density map associated with each snapshot $a_i$. The density field for a given snapshot was obtained as follows. To each snapshot $a_i$ we associate a specific comoving shell $[\chi_{i-1/2}, \chi_{i+1/2}]$ (see Appendix A for more details). We then select all of the particles that fall into the shell for that epoch, i.e. the $i$th dark matter particle in the $a$th snapshot, is accepted in the shell if $\chi_{i-1/2} < |x_i - x_0| < \chi_{i+1/2}$, where $x_i$ and $x_0$ are the coordinates of the $i$th dark matter particle and the observer, respectively. Note that if a given value of $\chi$ is larger than $L/2, 3L/2, 5L/2, \ldots$, then we apply periodic boundary conditions to produce replications of the cube to larger distances. If the particle is accepted, then we compute the angular coordinates $(\theta, \phi)$ for the particle, relative to the observer. Given these angular coordinates, we then find the associated HEALPix pixel and increment the counts in that pixel. The bottom panel of Fig. 4 shows the projected overdensity map for a thin redshift shell centred on $z = 0.3$. We note that it is hard, by eye, to note any apparent correspondence between the overdensity and temperature maps.

At the end we have 11 density maps between $z = 1.0$ and $z = 0.0$ that form concentric shells around the observer. These shells were then co-added using the weights given by our analytic fit to the redshift distribution of superclusters and supervoids (recall the solid line in the left panel of Fig. 1). The resulting co-added all-sky density maps are then smoothed from $N_{\text{side}} = 256$ to $N_{\text{side}} = 32$, and the positions of the $2n$, $n$ and $n/2$ most under- and over-dense pixels on this map are recorded. The number $n$ corresponds to a number density of extrema that is identical to that of real voids and superclusters under the footprint of SDSS DR6. Each of those extreme pixels on the $N_{\text{side}} = 32$ map is then projected back to the $N_{\text{side}} = 256$ map on a subset of
4.3 Validation tests of zHORIZON derived maps

Before we apply the analysis methods of G08 to our ISW and density maps, we first test the consistency of the maps themselves. To do this, we compute the angular auto-power spectra of the ISW temperature maps for each of the 8 zHORIZON runs. The left panel of Fig. 5 presents the ensemble-averaged temperature power spectrum for the ISW effect. The measurements from the simulations are represented by the solid black points. The prediction from linear theory is given by the solid red line. For multipoles in the range $5 < \ell < 70$, the agreement between the two is excellent. At low multipoles ($\ell < 5$) the absence of power in the simulation on scales larger than $L$ induces a low bias. Instead, on scales $\ell > 70$, the non-linear evolution of potentials substantially boosts the signal relative to linear by means of the Rees-Sciama effect.

We next compute the angular auto-power spectrum of the projected density contrast maps, with the projection extending from $z = 0.1$ up to $z = 1$ (middle panel of Fig. 5). In this case, the projected density angular power spectrum shows good agreement with the linear-theory expectations in the intermediate- and high-multipole range ($5 < \ell < 200$), and some hints for power deficit on the large scales/low $\ell$-s, which would probably be due to the lack of $k$ modes beyond the box size of the simulations.

Finally, the right panel of Fig. 5 compares the ISW - density cross-correlation estimated from the simulations with the linear theory. As for the other cases, there exists some power deficit at low multipoles due to finite volume effects in the simulations. At high multipoles the linear theory prediction lies above the simulations, this owes to the fact that in the deeply non-linear regime potentials do not decay, but grow with time through the Reese-Sciama mechanism, and hence this leads to a suppression of power (for further details see Smith et al. 2009). On intermediate angular scales the theoretical prediction is roughly $\sim 10$ per cent higher than the simulations, although with significant scatter. This slight mismatch is likely due to the construction of the weighted projected density field, since the ISW auto-spectra are in excellent agreement with the simulations.

4.4 Aperture analysis of the zHORIZON maps

Having validated the simulated maps, we now repeat the AP analysis. Since here we have both full-sky density and temperature maps, we prefer not to apply any sky mask. Thus, these predictions will not be affected by incomplete sky coverage. We repeat the steps described in §3 for finding the locations of the density peaks/troughs in each of the simulated smoothed maps. Then, as before, we apply the AP filters to the selected centroid positions for the 8 ISW maps from the zHORIZON simulations.

Figure 6 presents the results from this analysis. The square and circular symbols denote the results for our effective supercluster and supervoid regions, respectively. The blue, green and black colours correspond to the set of extreme pixels which have half, equivalent and double the angular number density of the real supervoids and superclusters found in G08’s analysis. We see that the peak of the average AP output has a temperature of the order $2 \mu$K, and occurs for apertures of scale $\sim 6 - 7^\circ$.

On comparison with the predictions from our Gaussian realisations, we find that the fully nonlinear ISW maps are in close agreement (c.f. §1.1). The are however small differences. The peak signal is shifted to slightly larger scales for the full nonlinear case. Also, the shape of the curves obtained from the zHORIZON simulations appears smoother than in the Gaussian simulation case, which shows dips and troughs that are absent in Fig. 5. We believe that these small differences are likely a consequence of the fact that the Gaussian realisations include intrinsic CMB noise and possess a sky-mask.

Actually, after applying the real sky masks to the simulated maps, we find that the peak amplitudes and the general shapes of the functions in Fig. 6 become distorted at the $\sim 10$ per cent level.

However, the most important point to note, is that on angular scales of the order $3 - 4^\circ$, the Gaussian and fully nonlinear simulations are in close agreement: the difference induced by adopting a slightly different cosmological model should introduce changes in the ISW amplitude at the 2 per cent level, and the ISW generated beyond $z = 1$ seems to have little impact as well. We thus conclude this section by noting that that the excess temperature signal found by G08, and now confirmed by us in §3, appears to be incompatible with the evolution of gravitational potentials in the standard ΛCDM model. Our results from both Gaussian realisations and ISW maps derived from the N-body sim-
Figure 5. (Left) Comparison of the average angular power spectra obtained from the zHORIZON-derived ISW maps (black circles) and the theoretical expectation (red solid line). The lack of low-$k$ modes causes a low bias in the low multipole range, and non-linear evolution introduces some visible power excess on the small scales. (Middle) Comparison of the average angular power spectra from the zHORIZON-derived density contrast maps (black circles) with the linear prediction (red solid line), for the redshift range $z \in [0.1, 1]$. The agreement with theory is again good on intermediate and small scales, but there seems to be again some slight low bias on the largest scales/lowest multipoles, showing some low bias for the redshift range $z \in [0.1, 1]$. Data from the simulations compare low to theoretical expectations on the large scales/low multipoles due to the finite box size, on the high multipoles due to non-linear evolution, and also show a slight ($\sim 10$ per cent) power deficit on intermediate multipoles due to the finite discretization of the line of sight into 11 shells.

5 SIGNIFICANCE, SYSTEMATICS AND ALTERNATIVE MODELS

5.1 Estimating the significance

The direct comparison of Fig. 2 and 3 reveals clear differences between the observed data and theoretical predictions. Not only is the amplitude of the maximum signal in the real data a factor of $\sim 5$ times larger than the average in the Gaussian realisations, but the dependence of the signal on the filter scale shows a different shape. More quantitatively, the results from the W-band WMAP data for an aperture size of 3.6°, are of the order $\sim 3.4 \sigma$ away from the superstructure simulation average, and $\sim 2.1 \sigma$ away from the average for the case of superclusters. In terms of probability, for an aperture scale of 3.6°, only 5 out of the 5000 realisations possessed an ISW signal, from subvoid regions, with a temperature decrement lower than the one found in real data, and 97 of the realisations for superclusters exceeded the value obtained for the real data. Taken at face value, this analysis seems to exclude the Gaussian ΛCDM hypothesis at $\sim 4\sigma$ significance. However, this is an a posteriori estimate, since we have neglected the fact that we also looked for a signal at other aperture scales.

If, for the W-band WMAP data, we include the measurements from the 15 different angular aperture scales between $1-20'$ and take into account their covariance, then the significance drops. Under the assumption of Gaussian statistics, we find that the WMAP outputs for voids produce a $X^2_{\text{voids}} = 23.5$ ($n_{\text{dof}} = 15$). The corresponding figure for superclusters is $X^2_{\text{superclusters}} = 26.6$ ($n_{\text{dof}} = 15$). If we treat these two constraints as being independent then their combination yields $X^2_{\text{both}} = 50.0$ ($n_{\text{dof}} = 30$). In terms of probability, this means that the WMAP data have a 0.012 probability (i.e. $< 2$ per cent chance or $\sim 2.2 \sigma$ under Gaussian statistics) of being consistent with the evolution of gravitational potentials in the ΛCDM model. If we consider the null hypothesis of no ISW signatures expected at all (for which stacking on voids and superclusters should leave no temperature decrement/increment), then the results lie at $2.6 \sigma$ away from this scenario.

We next study the dependence of the statistical significance on the number of substructures considered in the analysis. While the original catalogue of voids and superclusters of G08 contains 50 entries, we now repeat our tests after considering two subsamples containing only the first 30 and 40 objects. For these subsamples, the adopted values of the Gaussian threshold were $\nu = 2.87$ and 2.97. In these cases, the pattern found for the full catalogue is reproduced: the stacked voids give a temperature decrement of $\lesssim -10 \mu$K, at $\sim 3-3.5 \sigma$; the stacked superclusters give a temperature increment of $\gtrsim 7 \mu$K, at the level of $\sim 2.2-2.4 \sigma$. On comparison with Gaussian realisations, we find that, after considering all aperture radii, results for the first 40 superstructures are in lower tension with the outputs of Gaussian realisations (at the level of $< 3.0$ per cent or $1.9 \sigma$). This level of tension further decreases when considering only the first 30 superstructures ($\sim 27$ per cent or $0.6 \sigma$), showing that the tension of WMAP data wrt to Gaussian realisations relaxes as fewer structures are included in the analysis. This is somehow expected from the Gaussian realisations, for which the
statistical significance for the ISW increases with decreasing thresholds. This is in apparent contradiction with Table 1 of G08, where it is shown that the statistical significance of their ISW measurement at a scale of 4° decreases when increasing the number of structures from 50 (4.4σ) to 70 (2.8σ). In G08 it is argued that by considering more structures one may be diluting the signal by including unphysical structures, an extent that cannot be tested in our Gaussian maps since it is strictly associated to the algorithms identifying voids and superclusters in the galaxy catalogues.

In summary, according to our Gaussian simulations, the ∼ 4σ deviation wrt ΛCDM expectations found at a 3.6° aperture radius decreases to ∼ 2.2σ when including different filter apertures in the range [1°, 20°], and lies, in this case, 2.6σ away from the null (no ISW) case. While this tension relaxes when considering fewer structures, the significance of the detected signal seems to decrease when considering more than 50 voids and superclusters (see Table 1 of G08), in an opposite trend to what is suggested by our Gaussian ISW realisations.

We conclude that most of the significance of the G08 result is at odds with ISW ΛCDM predictions, both in amplitude and scale/aperture radius dependence, and that this tension considerably reduces when more aperture radii and structure sub-samples are considered in the analysis.

5.2 Tests for systematics

Given the high level of discrepancy existing between the pattern found at 3.6° aperture radius and ISW ΛCDM expectations, we next test the possibility of systematics in WMAP data giving rise to the observed signal.

- Rotation test: We first conduct a rotation test assessing the statistical significance of the AP outputs for a 3.6° scale. In this way, we probe the possibility of any other signal (apart from CMB) contributing to the uncertainty of the AP filter outputs and hence modifying the statistical significance found for WMAP data. We rotate in galactic longitude (in steps of 9°) the AP filter targets with respect to the positions of supervoids and superclusters. In the absence of systematics, this should provide AP outputs compatible with zero.

Figure 7 presents the results from this analysis. The blue circular symbols represent the supervoid regions and the red square symbols denote the superclusters. At zero rotation lag we clearly obtain a signal of higher amplitude than in any other rotation bin. We have verified that this signal does not arise as a consequence of a small subset of the supervoids/superclusters. Instead, the signal is approximately evenly distributed among all structures. From the sample of rotated bins only, the estimated significance for the 3.6° aperture is 4.1σ for voids, 2.7σ for superclusters, and 3.8σ combined. This is within 1–σ from the significance levels obtained with our Gaussian ISW realisations.

- Density-dependent contaminant: Another possible systematic is some combination of contaminants present in the superclusters that increases the emission in these structures in a frequency independent manner. This could happen if the CMB cleaning algorithms remove only the frequency varying part of the contaminant signal, but leave behind a DC level. In such a scenario, one might assume that the signal is linearly responding to fluctuations in the projected matter density. We incorporate this effect into our Gaussian realisations by substituting the total CMB map by a signal proportional to the projected matter density field in our Gaussian realisations. This should provide us with some idea of the scale-dependence for a contaminant of this nature.

Figure 8 presents the results from this exercise. The blue circular symbols represent the supervoid regions and the red square symbols denote the superclusters. At zero rotation lag we clearly obtain a signal of higher amplitude than in any other rotation bin. We have verified that this signal does not arise as a consequence of a small subset of the supervoids/superclusters. Instead, the signal is approximately evenly distributed among all structures. From the sample of rotated bins only, the estimated significance for the 3.6° aperture is 4.1σ for voids, 2.7σ for superclusters, and 3.8σ combined. This is within 1–σ from the significance levels obtained with the Gaussian realisations.

Figure 7. Rotation test on AP filter outputs for an aperture size of 3.6°. Blue circles (red squares) correspond to voids (superclusters).

Figure 8. Pattern induced versus AP filter scale by a contaminant following the local matter density.
Figure 9. Relative difference between full-sky ISW temperature maps for models with primordial non-Gaussianity and Gaussian models for flat ΛCDM universes. Top panel: presents \(\Delta T^{\text{ISW}}(f_{\text{local}}^{\text{NL}} = +100) - \Delta T^{\text{ISW}}(f_{\text{local}}^{\text{NL}} = 0)\). Bottom panel: presents the same but for \(\Delta T^{\text{ISW}}(f_{\text{local}}^{\text{NL}} = -100) - \Delta T^{\text{ISW}}(f_{\text{local}}^{\text{NL}} = 0)\). All maps were smoothed with a Gaussian filter of FWHM = 1.0°, which roughly corresponds to the scales at which the signal for the AP filters peaks. The large-scale temperature fluctuations appear slightly cooler/hotter in Universes with \(f_{\text{local}}^{\text{NL}}\) positive/negative.

- **Superstructure selection effects:** It might be argued that our identification of under- and over-dense regions in our simulated density maps does not match well the selection of supervoids and superclusters in the G08 data. Whilst in principle both approaches should generate the most under- and over-dense regions in volume limited samples of the universe, differences in the exact details of the ZOBOV and VOBOZ implementations may introduce subtle but important differences in the selection of regions. This would have an impact in the final definition and selection of targets for the AP filters. Properly addressing this issue would require a thorough implementation of the ZOBOV and VOBOZ algorithms to semi-analytic galaxy samples embedded...
in our simulations (and this goes beyond the scope of the current work). Having said this, the stability of our results with respect to the actual density peak threshold adopted, suggests that this would not critically affect our conclusions.

5.3 Primordial non-Gaussianity

In this section we explore whether the G08 result is compatible with a non-Gaussian distribution for the primordial potential perturbations. In particular, we consider the well known local model for primordial non-Gaussianity, characterized by a quadratic correction to the Gaussian Bardeen’s potential perturbation (see Komatsu et al. 2011 and references therein):

$$\Phi_{NG}(x) = \Phi_G(x) + f_{NL}^{local} [\Phi_G(x)^2 - \langle \Phi_G(x)^2 \rangle],$$  \hspace{1cm} (9)

where $\Phi_G(x)$ is the Gaussian potential perturbation after matter radiation equality, scaled in terms of units of $c^2$ to yield a dimensionless quantity. Following standard convention, $\Phi_{NG}(x) \equiv -\Phi^{\text{Newton}}(x)$ (i.e. the $\Phi$ in Eq. (1)). The term $\langle \Phi_G(x)^2 \rangle$ is subtracted to ensure that $\Phi_{NG}$ is a mean zero field. In linear theory the typical fluctuations are of the order $\Phi_{NG} \sim 10^{-5}$, and so the non-Gaussian corrections are of the order $\sim 0.1 f_{NL}^{local} / (100) (\Phi_G/10^{-5})^2$.

In order to explore the observable consequences of such a modification, we have generated a set of simulated ISW maps with Gaussian initial conditions, i.e. $f_{NL}^{local} = 0$, and with non-Gaussian initial conditions $f_{NL}^{local} = \{+100, -100\}$. These maps were generated from N-body simulations seeded with Gaussian and non-Gaussian initial conditions following the methodology of Appendix A. The simulations that we employ were fully described in Desjacques et al. (2009). In brief, these were performed using Gadget-2, and followed $N = 1024^3$ dark matter particles in a box of size $L = 1600 h^{-1} \text{Mpc}$. The cosmological model of the simulations was consistent with the WMAP5 data (Komatsu et al. 2009). We use a sub-set of these simulations that were used elsewhere for gravitational lensing analysis (Marian et al. 2011; Hilbert et al. 2012). The simulations were set up to have the same initial random phases for all three models, this enables us to cancel some of the cosmic variance and so permit us to better explore the model differences.

The top panel of Fig. 3 presents the between the ISW temperature maps in a Universe with $f_{NL}^{local} = +100$ and $f_{NL}^{local} = 0$. The bottom panel shows the same but for the case $f_{NL}^{local} = -100$ and $f_{NL}^{local} = 0$. Note that all of the maps were smoothed with a Gaussian filter of FWHM = 1° before being differenced. Note also that we have only included the ISW contributions between $z = 0.0$ and $z = 1.0$. Clearly, the presence of primordial non-Gaussianities can induce shifts in the temperatures of the peaks and troughs of the distribution. However, these shifts are modest for $f_{NL}^{local} = \pm 100$, leading to changes that are $< 1 \mu\text{K}$. This suggests that values of $f_{NL}^{local}$ on the order of $\sim 1000$, might be able to explain the AP analysis of the WMAP results. However, such large values for $f_{NL}^{local}$ would be grossly inconsistent with the values of $f_{NL}^{local}$ obtained from the CMB temperature bispectrum, which currently gives $-10 < f_{NL}^{local} < 74$ (95% C.L. Komatsu et al. 2011). It therefore seems unlikely that the scale-independent local model of primordial non-Gaussianity is the correct explanation for the excess signal.

6 CONCLUSIONS

In this work we have studied the imprint of superclusters and supervoids in the temperature map of the CMB from the WMAP experiment. Our work further explores the signature first detected in Granett et al. (2008; G08).

In (2) we theoretically showed that if G08 had applied a standard angular cross-power spectrum analysis of the superstructures they found in the SDSS LRG data, then the expected significance for a $\Lambda$CDM model should have been $< 1.5 \sigma$.

In (3) we cross-checked the G08 analysis directly and found identical conclusions: on scales $\sim 3.6^\circ$ there was a $\sim 4 \sigma$ detection significance for excess signal associated with the supervoids and superclusters.

In (4) we performed a series of tests exploring whether these findings are consistent with the standard $\Lambda$CDM model. Gaussian Monte-Carlo realisations of the ISW effect and the LSS were unable to produce such large signals. We then investigated whether this was a consequence of our simplified Gaussian realisations. We did this by generating fully non-linear ISW maps from large volume N-body simulations. These simulated maps confirmed the findings of the simpler Gaussian realisations.

In (5) we used the Gaussian Monte-Carlo realisations to explore the significance of the deviations from the $\Lambda$CDM model found in the WMAP data. We found that for aperture photometry analysis of the maps on scales $3.6^\circ$, results from WMAP data are lying about $\sim 4 \sigma$ away from $\Lambda$CDM expectations. However, on taking into account the 15 aperture radius of 3 $\sigma$ and the null (no ISW) scenario where structures leave no signatures on the CMB at the linear level. When including fewer structures in the analysis, the tension dropped further, and results for only 30 voids and superclusters were compatible both with $\Lambda$CDM expectations (at $0.6 \sigma$) and the null (no ISW) scenario (at $1.3 \sigma$). Our simulations also suggested that the ISW significance should increase when more structures were included in the analysis, in apparent contradiction with the findings of G08. Hence, most of the detected signal appeared associated to the full set of 50 superstructures and an aperture radius of 3 $^\circ$.

We investigated whether the observed pattern at a radius of $3.6^\circ$ could be caused by a systematic error in the cleaning of foregrounds in the WMAP data. We found that if the signal were to be caused by an approximately frequency-independent emission tracing the density field, then the resulting angular dependence would be very different to the measured shape found in the WMAP data.

We next explored whether the observed signal at $3.6^\circ$ could be generated by primordial non-Gaussianities. We considered the local model, characterized by a quadratic correction to the primordial potential perturbations, with the coupling parameter $f_{NL}^{local}$. We found that, for $f_{NL}^{local}$ positive/negative, asymmetric shifts in ISW temperature maps arise. However, for the values of $f_{NL}^{local} = \pm 100$, the changes were $< 1 \mu\text{K}$ (after smoothing the maps down to degree scales). Thus values of $f_{NL}^{local}$ an order of magnitude higher would be required to explain the G08 result, and they would...
be clearly inconsistent with current constraints on $f_{\text{NL}}^{\text{local}}$ from WMAP.

It is possible that the G08 result may also be explained by other more exotic scenarios, e.g., non-Gaussianity arising from the presence of a non-zero primordial equilateral or orthogonal model bispectrum (a consequence of non-standard inflationary mechanisms); alternatively it might arise as a direct consequence of modifications to Einstein’s general theory of relativity, [Jain & Khoury(2010)]. However, more conservative scenarios involving some combination of artifacts and/or systematics cannot yet be fully discarded.

In the future, we will look with interest to the results from the Planck satellite as to whether this signal represents a data artifact, or whether it constitutes a genuine challenge to the $\Lambda$CDM model and a window to new cosmological physics.

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APPENDIX A: FULL SKY ISW MAPS FROM N-BODY SIMULATIONS

In this section we aim to construct full-sky ISW maps using a suite of N-body simulations. Our approach is similar to that described in Cai et al. (2014), but with some modifications. To be more precise, we aim to compute the line-of-sight integral Eq. (1), but taking into account the full nonlinear evolution of $\Phi$. The steps we take to achieve this are described below.

A1 Determining $\Phi$

In order to obtain $\Phi$ directly from the N-body simulations, we make use of Eq. (4), which tells us that our desired quantity can be determined from knowledge about $\delta(k,a)$ and $\delta(k,a)$. In simulations, measuring $\delta(k,a)$ is relatively straightforward, whereas its time derivative is more complicated. As was shown by Seljak (1996), this latter quantity may be obtained from the perturbed continuity equation (Peebles 1980):

$$\nabla \cdot [1 + \delta(x;t)] \, v_p(x;t) = -\dot{a}(t) \delta(x;t) \, , \quad \text{(A1)}$$

where $v_p(x;t)$ is the proper peculiar velocity field. If we define the pseudo-peculiar momentum field to be,

$$p(x;t) \equiv [1 + \delta(x;t)] \, v_p(x;t) \, , \quad \text{(A2)}$$

then in Fourier space we may solve the continuity equation directly to find

$$\delta(k;t) = \frac{i \mathbf{k} \cdot \mathbf{p}(k;t)}{a(t)} \, . \quad \text{(A3)}$$

Hence, our final expression becomes,

$$\dot{\Phi}(k;t) = \mathcal{F}(k) \left[ \frac{H(t)}{a(t)} \delta(k;t) - \frac{i \mathbf{k} \cdot \mathbf{p}(k;t)}{\alpha^2(t)} \right] \, , \quad \text{(A4)}$$

where we defined the function

$$\mathcal{F}(k) \equiv \frac{3}{2} \Omega_m \left( \frac{H_0}{k} \right)^2 \, . \quad \text{(A5)}$$

Thus in order to estimate $\dot{\Phi}$, we simply require estimates of both the density field and pseudo-peculiar momentum field in Fourier space.

The dark matter density field in an N-body simulation can be written as a sum of Dirac delta functions,

$$\rho(x) = \sum_{i=1}^{N} m_i \delta^D(x - x_i) \, , \quad \text{(A6)}$$

where $N$ is the number of particles and $m_i$ is the mass of the $i$th particle, and we take all particles to have equal mass. The density field averaged on a cubical lattice can then be obtained through the convolution,

$$\rho_g(x_{ijk}) = \frac{1}{V_W} \int d^3 x \rho(x) W(x_{ijk} - x) \, ;$$

$$= \frac{m}{V_W} \sum_{i=1}^{N} W(x_{ijk} - x_i) \, . \quad \text{(A7)}$$

where $x_{ijk}$ labels the lattice point, $W$ represents the dimensionless window function of the mass assignment scheme. This window function is normalized such that $V_W = \int d^3 x W^2(x - x')$. The filter function $W$ that we adopt throughout is the ‘cloud-in-cell’ charge assignment scheme (Hockney & Eastwood 1988). Hence, our estimate for the density fluctuation is

$$1 + \delta(x_{ijk}) = \frac{1}{N} \sum_{i=1}^{N} W(x_{ijk} - x_i) \, ,$$

$$= N_{\text{cell}} \frac{1}{N} \sum_{i=1}^{N} W(x_{ijk} - x_i) \, . \quad \text{(A8)}$$

where $N_{\text{cell}} = V_W / V_W$ is the total number of grid cells.

The pseudo-momentum field may be estimated in a similar fashion. For convenience we write,

$$p = [1 + \delta(x)] \, u(x) a(t) \, , \quad \text{(A9)}$$

where $u = v_p/a$ is the comoving peculiar velocity field. The particle momentum field is then written as

$$[(1 + \delta) u](x) = \frac{V_W}{N} \sum_{i=1}^{N} \delta^D(x - x_i) u_i \, . \quad \text{(A10)}$$

This may be convolved with the mass assignment scheme to obtain the mesh averaged quantity

$$[(1 + \delta) u](x_{ijk}) = \frac{1}{V_W} \sum_{i=1}^{N} u_i W(x_{ijk} - x_i) \, . \quad \text{(A11)}$$

Thus our estimate for the pseudo-momentum field is

$$\hat{p}(x_{ijk}) = \frac{a(t) N_{\text{cell}}}{N} \sum_{i=1}^{N} u_i W(x_{ijk} - x_i) \, . \quad \text{(A12)}$$
The density Fourier modes were then estimated using the publicly available FFTW routines (Johnson & Frigo 2008), and each resulting mode was corrected for the convolution with the mass-assignment window function. For the CIC algorithm this corresponds to the following operation:

$$\delta_d(k) = \delta_g(k)/W_{\text{CIC}}(k),$$

where

$$W_{\text{CIC}}(k) = \prod_{i=1,3} \left\{ \sin \left[ \pi k_i/2k_{Ny} \right]/\pi k_i/2k_{Ny} \right\}^2$$

and where sub-script d and g denote discrete and grid quantities, and where $k_{Ny} = \pi N_g/L$ is the Nyquist frequency, and $N_g$ is the number of grid cells (Hockney & Eastwood 1988).

To obtain the real space $\Phi(x,t)$, we solved for $\Phi(k,t)$ in Fourier space using Eq. (A4), set the unobservable $k = 0$ mode to zero, and inverse transformed back to real space.

A2 Reconstructing the light-cone for $\Phi$

We now wish to construct the past light-cone for the evolution of $\Phi$, however we only have a finite number of snapshots of the particle phase space from which to reconstruct this. It is usually a good idea to space snapshots logarithmically in expansion factor, and for simplicity we shall now assume that to be true. The light-cone can then be constructed as follows:

- Find $\Phi(x_{ijk},a_i)$ for every output $t$ on a periodic cubical lattice, using the techniques described in Appendix A1.
- Place an observer at the exact centre of the simulation cube, $x_0$, and compute the comoving distances from the observer to the expansion factors, $a_{i-1/2}$, $a_i$, and $a_{i+1/2}$, and label these distances $\chi_{i-1/2}$, $\chi_i$ and $\chi_{i+1/2}$. Here, $\log a_{i \pm 1/2} = \log a_i \pm \Delta \log a/2$, 

with $\Delta \log a$ being the logarithmic spacing between two different expansion factors. The comoving distance from the observer at $a_0$ to expansion factor $a$ is given by:

$$\chi(a) = \int^{\log a_0}_{\log a} \frac{cd\alpha}{a^2 H(a)}.$$ 

Hence, the intervals $[\chi_{i-1/2}, \chi_{i+1/2}]$ form a series of concentric shells centred on the observer.
- Construct a new lattice for the $\Phi$ values on the light cone. This is done by associating to each snapshot $a_i$, a specific comoving shell $[\chi_{i-1/2}, \chi_{i+1/2}]$, and taking only those values for $\Phi(x_{ijk},a_i)$ that lie within the shell: i.e. if $\chi_{i-1/2} < |x_{ijk} - x_0| \leq \chi_{i+1/2}$, then $\Phi(x_{ijk},a_i)$ is accepted onto the new grid. Note that if a given value of $\chi$ is larger than $L/2$, $3L/2$, $5L/2$, . . . , then we use the periodic boundary conditions to produce replications of the cube.

A3 Computing the ISW line-of-sight integral

Having constructed the backward lightcone for $\Phi$, we may now compute the line-of-sight integral for the ISW effect through Eq. (1). In fact we use a slightly different form of this equation by transforming the integration variable from $t$ to $\log a$: i.e.

$$\frac{\Delta T(n)}{T_0} = \frac{2}{c^2} \int_{\log a_0}^{\log a_n} d \log a \frac{\Phi(n,\chi)}{H(a)}.$$ (A15)

The above expression can then be discretized to give,

$$\frac{\Delta T(n)}{T_0} \approx \frac{2}{c^2} \sum_{i=0}^{M} \Delta \log a_i \frac{\hat{\Phi}(n,a_i)}{H(a_i)}.$$ (A16)

If we take $\Delta \log a$ to be constant, then this becomes,

$$\frac{\Delta T(n)}{T_0} \approx 2 \Delta \log a \sum_{i=0}^{M} \frac{\hat{\Phi}(n,a_i)}{H(a_i)}.$$ (A17)

In evaluating the above expression, we take the number of intervals to be as large as desired, but always evaluating $H(a_i)$ exactly through the expression (Dodson 2003; Weinberg 2008),

$$H^2(a) = H_0^2 \left[ \Omega_{\Lambda 0} + \Omega_m a^{-3} - (\Omega_{\Lambda 0} + \Omega_m - 1)a^{-2} \right],$$ (A18)

which is valid in the matter dominated epoch for the ΛCDM model. Whereas, for $\Phi(a)$, we employ the light cone derived form from the previous subsection, but interpolate the value off the 3D mesh using a CIC like scheme. That is:

$$\Phi(x,a) = (1 - h_z)(1 - h_y)(1 - h_x)\Phi(x_{i,j,k}) + (1 - h_x)h_y\Phi(x_{i,j,k+1}) + \ldots + h_z h_y h_x \Phi(x_{i+1,j+1,k+1})$$ (A19)

where $h_x, h_y, h_z$ are the x-, y-, and z-coordinate separations of the evaluation point $x$ and the position vector for lattice point $(i,j,k)$, in units of the inter-lattice separation.

In making this separation of the evolution of $H(a)$ and $\Phi$, we are effectively assuming that $\Phi$ evolves very slowly over the time interval between snapshots. This is a reasonable assumption on large scales, since, as discussed in [2], the time derivative is close to zero for most of the evolution of the Universe and only weakly evolving after this at later times. On smaller scales this may be a less reasonable approximation, however, we are still using the fully nonlinear gravitational potential field.