Nonisothermal decomposition and safety parameters of HNIW/TNT cocrystal

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To explore the thermal decomposition behavior and evaluate the thermal safety of the cocrystal 2,4,6,8,10,12-hexanitrohexaazaisowurtzitane (HNIW)/2,4,6-trinitrotoluene (TNT), its thermal and kinetic behaviors were studied by differential scanning calorimetry (DSC) technique. With the help of onset temperature ($T_o$) and maximum peak temperature ($T_p$) from the non-isothermal DSC curves of HNIW/ TNT cocrystal at different heating rates ($\beta$), the following were calculated: the value of specific heat capacity ($C_p$) and the standard molar enthalpy of formation ($\Delta_f H_m^\ominus$, s, 298.15 K), the apparent activation energy ($E_A$ and $E_C$) and pre-exponential constant ($A_0$) of thermal decomposition reaction obtained by Kissinger’s method and Ozawa’s method, density ($\rho$) and thermal conductivity ($\lambda$), the decomposition heat ($Q_d$, as half-explosion heat), Zhang–Hu–Xie–Li’s formula, Smith’s equation, Friedman’s formula, Bruckman–Guillet’s formula, Frank–Kamenetskii’s formula and Wang–Du’s formulas, the values ($T_{eo}$ and $T_{po}$ of $T_o$ and $T_p$ corresponding to $\beta \to 0$, thermal explosion temperature ($T_{eo}$ and $T_{bp}$), adiabatic time-to-explosion ($t_{aad}$), 50% drop height ($H_{50}$) for impact sensitivity, critical temperature of hot-spot initiation ($T_{cr}$), thermal sensitivity probability density function ($S(T)$) vs. temperature ($T$) relation curves with radius of 1 m and ambient temperature of 300 K, the peak temperature corresponding to the maximum value of $S(T)$ vs. $T$ relation curve ($T_{S(T)_{max}}$), safety degree (SD) and critical ambient temperature ($T_{acr}$) of thermal explosion. Results show that the kinetic equation describing the exothermic decomposition reaction of HNIW/TNT cocrystal is $\ln(a) = -\frac{3}{2}(1-a)\left[-\ln(1-a)\right]^3 \exp(-2.8318 \times 10^{15}/T)$. The following thermal safety parameters for the HNIW/TNT cocrystal are obtained: $T_{eo} = 464.45$ K, $T_{po} = 477.55$ K, $T_{be} = 472.82$ K, $T_{bp} = 485.89$ K, $t_{aad} = 4.40$ s, 4.42 s, and 4.43 s for $n = 0, 1$, and 2, respectively; $T_{cr} = 531.90$ K, $H_{50} = 19.46$ cm; and the values of $T_{acr}$, $T_{S(T)_{max}}$ SD and $P_{TE}$ are 469.69 K, 470.58 K, 78.57% and 21.43% for sphere; 465.70 K, 470.58 K, 78.17% and 21.83% for infinite cylinder, and 459.39 K, 464.26 K, 77.54% and 22.46% for infinite flat.

1 Introduction

High-density energetic materials (HDEMs) show great potential use in the military field, e.g., as propellants, pyrotechnics, explosives and gas generators. Along with the fast development of the energetic materials (EMs), the demand is increasing for the insensitive EMs; specifically, it is necessary to generate high-energy EMs with low sensitivity. As is known, the conflicts between increasing chemical energy and decreasing the sensitivity are severe. Many efforts have been made to improve the power and insensitivity of EMs, and synthesis of new compounds and modification of existing materials are the primary methods used. Co-crystallization is an effective and convenient means to improve the performance of materials, and it has drawn wide attention among researchers. Co-crystallization, combining two or more neutral molecules through non-covalent interactions, could compromise the merits of the individual substance, and one of the energetic compounds has shown the ability to alter undesirable material properties, such as high sensitivity or low density. 2,4,6,10,12-Hexanitrohexaazaisowurtzitane (HNIW) is the most powerful explosive owing to its high density (>2.0 g cm$^{-3}$), good oxygen balance (~10.94%) and high detonation velocity (9400 m s$^{-1}$), but its high sensitivity toward external stimuli constrains its application. 4,6-Trinitrotoluene (TNT) is an extensively used explosive with good stability. Bolton successfully prepared the HNIW–TNT cocrystal [in a 1 : 1 stoichiometry] in 2011, which featured insensitivity and high energy. The nonisothermal decomposition behaviors and thermal safety parameters of EMs play vital roles in theoretical studies and engineering applications, providing significant guidance to their further applications and industrial production. In recent years, reports of the HNIW–TNT cocrystal have been...
concentrated on its synthesis, characterization, atomistic simulation and reactive molecular dynamics,16–22 but there is little literature reported about the thermal behaviors and thermal safety parameters of HNIW-TNT cocrystal. Before HNIW-TNT cocrystal can reach practical application, much work should be done for a more comprehensive understanding of this material. To add to these studies, herein, the non-isothermal decomposition behaviors and detailed thermal safety parameters of HNIW-TNT cocrystal are described. The HNIW-TNT cocrystal was prepared and characterized. Its non-isothermal decomposition was studied by differential scanning calorimetry (DSC), and the thermal safety parameters of HNIW-TNT cocrystal, including the self-accelerating decomposition temperature (Tₐₑₐₜ), the critical temperature of thermal explosion (Tₑₓ), and the adiabatic time-to-explosion (tₐₑₐₜ) were also calculated with the experimental data from non-isothermal decomposition. Moreover, the 50% drop height of impact sensitivity (Hₛₕₒ), the critical temperature of hot-spot initiation caused by impact (Tₐₑᵣₑ), the safety degree (SD), the critical thermal explosion ambient temperature (Tₑₐₑₜₑ) and thermal explosion probability (Pₑₓ) were also obtained.

2 Experimental

2.1 Caution

General caution: title compound is a hazardous material, explosions of which may occur in certain conditions. Although we had no difficulties during the experiments and in handling the compounds, appropriate safety precautions such as the use of safety glasses, face shields and horn spoons should be taken, especially when the compounds are prepared at a large scale.

2.2 Preparation

HNIW/TNT cocrystal was prepared and purified according to the literature method.19 It was kept in a vacuum desiccator before use. The structure of HNIW/TNT cocrystal was characterized by infrared spectroscopy (IR) and elemental analysis. IR (KBr): 3111, 3024 (CH), 1599, 1339, 1259, 943, 885 (NO₂), 1088, 1059 (N–N), 831, 752, 721 (skeleton ring) cm⁻¹. Anal. calc’d (%) for C₁₃H₁₁N₁₅O₁₈: C 23.47, N 31.58, H 1.67; found (%) C 23.55, N 32.01, H 1.59. High-performance liquid chromatography (HPLC; LC-20AD, Shimadzu Corporation, Japan) was used to confirm the content of HNIW and TNT in the HNIW/TNT cocrystal, with a Phenomenex C₁₈ analytical column (5.0 μm, 150 mm × 4.6 mm) at 298.15 K column temperature and the detection wavelength of 254 nm. The results demonstrate that the mole ratio of HNIW to TNT is 1 : 1 in the above prepared HNIW/TNT cocrystal.

2.3 Differential scanning calorimetry

The DSC experiments for the title compound were performed using a Q2000 apparatus (TA, USA) under nitrogen atmosphere at a flow rate of 50 ml min⁻¹. About 0.6 mg of sample was sealed in an aluminum pan, and the heating rates used were 2.5, 5.0, 10.0, 15.0 and 20.0 K min⁻¹ from ambient temperature to 773.15 K. DSC curves obtained under the same conditions overlapped with each other, indicating that the reproducibility of the tests was satisfactory.

3 Results and discussion

3.1 Standard enthalpy of combustion

The standard combustion enthalpy of the title compound, ΔHₑₘ (HNIW/TNT cocrystal, s, 298.15 K) was derived from the combustion enthalpy change of the following ideal combustion reaction (1) at 298.15 K and 100 kPa,

\[
C_{13}H_{11}N_{15}O_{18}(s) + 15.75O_2(g) \rightarrow 13CO_2(g) + 5.5H_2O(l) + 7.5N_2(g).
\]

and calculated by Hess’s law according to the thermochemical eqn (2),

\[
\Delta H_m^\circ(TNT, s, 298.15 K) = 13\Delta H_m^\circ(CO_2, g, 298.15 K) + 5.5\Delta H_m^\circ(H_2O, l, 298.15 K) - \Delta H_m^\circ(HNIW/TNT cocrystal, s, 298.15 K),
\]

where ΔH_m^\circ(CO_2, g, 298.15 K) = -(393.51 ± 0.13) kJ mol⁻¹, ΔH_m^\circ(H_2O, l, 298.15 K) = -(285.83 ± 0.042) kJ mol⁻¹, and ΔH_m^\circ(HNIW/TNT cocrystal, s, 298.15 K) = 324.445 ± 0.149 kJ mol⁻¹, determined through a thermochemical cycle, as reported elsewhere; the result obtained is -(7012.14 ± 3.42) kJ mol⁻¹.

3.2 Standard energy of combustion

The standard energy of combustion of the title compound ΔU (HNIW/TNT cocrystal, s, 298.15 K) was calculated by the following eqn (4):

\[
\Delta U = \Delta H_m^\circ + \Delta nRT
\]

where \( \Delta H_m^\circ = -(7012.14 ± 3.42) \text{ kJ mol}^{-1} \), \( \Delta n \) is the total amount in mole of gases present as products or as reactants, \( \Delta n = 13 + 7.5 - 15.75 = 4.75, R = 8.314 \text{ J K}^{-1} \text{ mol}^{-1} \), and \( T = 298.15 \text{ K} \). The result is -(7023.914 ± 3.42) kJ mol⁻¹.

3.3 The nonisothermal decomposition behavior of HNIW/TNT cocrystal

A typical DSC curve at a heating rate of 5.0 K min⁻¹ for HNIW/TNT cocrystal is shown in Fig. 1. The curve consists of one endothermic peak and one exothermic peak. The endothermic peak at 413.52 K is the phase change from solid to liquid. The exothermic peak is the decomposition reaction of HNIW/TNT cocrystal; the \( T_p \) is 490.61 K, and the \( T_e \) is 479.32 K.
3.4 Thermal conductivity (\(\lambda\))

According to the relationship between specific heat capacity at constant pressure \(C_p\) and specific heat capacity at constant volume \(C_v\) as \(C_p = 0.83C_v\) and substituting the values of \(M\) of 665.32 and \(a, b, c\) and \(d\) in eqn (5) into eqn (6),

\[
C_v = \left( \frac{3}{2} \right) \frac{R(a + b + c + d)}{M} \left[ 1 + \frac{2c}{(4a + b)(a + b + c + d)} - \frac{2a^2}{(4a + b)(a + b + c + d)^2} \right]
\]

we obtain \(C_p = 1.01\ J\ g^{-1}\ K^{-1}\), which is in accordance with our experiment results, determined by a continuous \(C_p\) mode of Micro-DSC III and will be reported elsewhere.

By replacing the values of \(C_p\) of 1.01 \(J\ g^{-1}\ K^{-1}\), \(\rho\) of 1.844 \(g\ cm^{-3}\), \(T_m\) of 413.52 K and \(M\) of 665.32 into eqn (7),

\[
\lambda = \frac{3.728 \times 10^5 \rho}{T_m^{0.3652} M^{0.2158}}
\]

the value of \(\lambda\) of 0.168 W (m K)\(^{-1}\) was obtained.

3.5 Explosion properties

By substituting the values of \(a, b, c\) and \(d\) in \(C_{NH_2O_2}N_{13} = C_{13}H_{11}O_{18}N_{15}\), \(\rho = 1.844\ g\ cm^{-3}\), \(\Delta H_{\text{in}} = 324.445\ kJ\ mol^{-1}\) into Kamlet–Jacobs eqn (8)–(12), the values of \(D\) of 8.624 km s\(^{-1}\), \(P\) of 33.89 GPa, \(N\) of 0.0289 mol g\(^{-1}\), \(M_k\) of 30.34 g mol\(^{-1}\), and \(Q\) of 618.471 J g\(^{-1}\) were obtained.

\[
D = 1.01(NM^{1/2}Q^{1/2})^{1/2}(1 + 1.30\rho)
\]

\[
P = 1.558N\rho M^{1/2}Q^{1/2}
\]

\[
N = \frac{\rho + 2d + 2c}{4M}
\]

3.6 Analysis of kinetic data for the main exothermic decomposition reaction of HNIW/TNT cocrystal

Two isoconversional methods [eqn (16) and (17)] were used to obtain the kinetic parameters (the apparent activation energy \(E_a\) and pre-exponential constant \(A\)) of the main exothermic decomposition reaction for the title compound:

**Differential method.** Kissinger equation\(^{27}\)

\[
\ln \left( \frac{\beta}{T^p} \right) = \ln \frac{A_k R}{E_k} - \frac{E_k}{R} \frac{1}{T^p}
\]

**Integral method.** Ozawa equation\(^{28}\)
where \( \alpha \) is the degree of reaction, \( T \) the absolute temperature, \( E \) the apparent activation energy, \( \beta \) the heating rate, \( R \) the gas constant, \( T_p \) the DSC curve peak temperature, and \( A \) the pre-exponential factor.

From the original data in Table 1, \( E_k \) obtained by Kissinger’s method\(^{37} \) is determined to be 239.40 kJ mol\(^{-1} \). The pre-exponential constant \( (A) \) is \( 10^{23.50} \) s\(^{-1} \). The linear correlation coefficient \( (r_k) \) is 0.9969. The value of \( E_0 \) obtained by Ozawa’s method\(^{26} \) is 233.45 kJ mol\(^{-1} \). The value of \( r_0 \) is 0.9971. The value of \( E_{co} \) obtained by \( T_m \) vs. \( \beta \) relation is 222.08 kJ mol\(^{-1} \). The value of \( r_{co} \) is 0.9946.

By substituting the experimental data, \( \beta_i, T_i \) and \( a_i, i = 1, 2, \ldots n \), listed in Table 2 from DSC curves at different heating rates into eqn (18), the values of \( E_0 \) for any given value of \( \alpha \) were obtained and are shown in Fig. 2. The average value of \( E_0 \) in the \( \alpha \) range of 0.10 to 0.90 in Fig. 2 is in good agreement with the calculated values obtained by Kissinger’s method and Ozawa’s method. The \( E \) values calculated using eqn (18)\(^{39} \) are used to check the validity of activation energy by the other methods.

\[
\Omega_i(E_0) = \min \left\{ \sum_{i=1}^{n} \sum_{j=1}^{n} \beta \beta_i I(E_0, T_{ai}) - n(n-1) \right\}
\] (18)

where the \( I(E_0, T_{ai}) \) integral is obtained taking the Senu-\( Y \)ang-Yang approximation calculation for approximation of 3\(^{rd} \) degree: \( I_{S-Y} (E, T) = \left[ T^{a - \frac{u^2 + 10u + 18}{u^3 + 12u^2 + 36u + 24}} \right] \) where \( u = \frac{E}{RT} \).

The data \( (\beta, T, a_i, i = 1, 2, \ldots) \) in the range of \( \alpha \) of 0.10–0.90 and 47 kinetic model functions\(^{19} \) were input to following eqn (19)–(23) to obtain the values of \( E \) and \( A \) from a single non-isothermal DSC curve.

Ordinary-integral equation\(^{30} \)

\[
\ln \left[ \frac{G(0)}{T^2} \right] = \ln \left[ \frac{AR}{\beta E} \left( 1 - \frac{2RT}{E} \right) \right] - \frac{E}{RT}
\] (19)

Universal integral equation\(^{31} \)

\[
\ln \left[ \frac{G(0)}{T - T_0} \right] = \ln \frac{A}{\beta} - \frac{E}{RT}
\] (20)

MacCall–Tanner equation\(^{32} \)

\[
\log[G(0)] = \log \left( \frac{AE}{RT} \right) - 0.4828E^{0.4357} - \frac{0.449 + 0.217E}{0.001} \frac{1}{T}
\] (21)

Satava–Sestak equation\(^{33} \)

\[
\log G(0) = \log \left( \frac{AE}{RT^2} \right) - 0.4828E^{0.4357} - \frac{0.449 + 0.217E}{0.001} \frac{1}{T}
\] (22)

Agrawal equation\(^{34} \)

\[
\ln \left[ \frac{G(0)}{T^2} \right] = \ln \frac{AR}{\beta E} \left( 1 - \frac{2RT}{E} \right) - \frac{E}{RT}
\] (23)
3.7 Heat-temperature quotient for the exothermic decomposition of HNIW/TNT cocrystal

The exothermic peak in Fig. 1 is caused by the decomposition reaction. Heat-temperature quotient $\Delta S_d$ of the process equals to:

$$\Delta S_d = \frac{Q_d}{T_{p0}} = \frac{Q_d}{T_{p0}} = (-2057.41 \text{ kJ mol}^{-1})/477.55 \text{ K} = 4.308 \text{ kJ mol}^{-1} \text{ K}^{-1} \quad (26)$$

In eqn (26), $Q_d$ is the heat of decomposition reaction, which is defined as $Q_d = 0.5Q$, i.e., $Q_d$ is the half-chemical energy (heat) of detonation. For HNIW/TNT cocrystal, $Q_d = 0.5Q = 3092.36 \text{ J g}^{-1}$, and $T_{p0}$ is the peak temperature $T_p$ corresponding to $\beta \rightarrow 0$.

3.8 Self-accelerating decomposition temperature $T_{SADT}$

Setting $T_e$ as the onset temperature and $T_p$ as the peak temperature, and defining $T_{eo}$ or $p_0$ as the value of $T_e$ or $p$ corresponding to $\beta \rightarrow 0$ and $T_e$ as the self-accelerating decomposition temperature $T_{SADT}$, we have:

$$T_{eo} = T_{p0} + b_1 + c_1 \beta^2 + d_1 \beta^3, \quad i = 1, 2, \ldots, L \quad (27)$$

and

$$T_{eo} = T_{SADT} \quad (28)$$

Replacing the experimental data: $b_1, T_{eo}, T_{p0}, i = 1, 2, \ldots, 5$ in Table 1 into eqn (27), the values of $T_{eo}$ of 464.45 K and $T_{p0}$ of 477.55 K are obtained. The $T_{SADT}$ value of 464.45 K is obtained by eqn (28).

3.9 The critical temperature of thermal explosion ($T_b$)

The critical temperature of thermal explosion ($T_b$) is an important parameter in evaluating the safety and elucidating transition tendency from thermal decomposition to thermal explosion for small-scale EMs.

For HNIW/TNT cocrystal, the values of $T_b$ obtained by the Zhang–Hu–Xie–Li equation [eqn (29)] taken from ref. 35 using the values of $T_{eo}$ (464.45 K) and $T_{p0}$ (477.55 K) and the values of $E_{oe}$ (222.08 kJ mol$^{-1}$) and $E_{op}$ (235.45 kJ mol$^{-1}$) are 472.82 and 485.89 K, respectively:

$$T_{bed(or pb)} = \frac{E_{oe} or op - \sqrt{E_{oe} or op^2 - 4E_{oe} or opRT(0 or pb)}}{2R} \quad (29)$$

In comparison with RDX for $T_{bp} = 454.08 \text{ K}$, the high value of $T_b$ shows that it is difficult for the transition from thermal decomposition to thermal explosion to take place.

3.10 Thermodynamic parameters of activation reaction

The entropy of activation ($\Delta S^*$), enthalpy of activation ($\Delta H^*$), and Gibb’s free energy of activation ($\Delta G^*$) corresponding to $T = T_{p0} = 477.55 \text{ K}, E = E_K = 239 400 \text{ J mol}^{-1}$, and $A = A_K = 10^{23.50}$ obtained by eqn (30)-(32) are $192.74 \text{ J mol}^{-1}$ K$^{-1}$, 235.43 kJ mol$^{-1}$ and 143.39 kJ mol$^{-1}$, respectively. The positive value of $\Delta G^*$ indicates that the exothermic decomposition reaction for HNIW/TNT cocrystal must proceed under the heating condition.

$$Ae^{-E/RT} = \frac{k_BT}{h}e^{-\Delta G^*/RT} \quad (30)$$

$$\Delta H^* = E - RT \quad (31)$$

$$\Delta G^* = \Delta H^* - T\Delta S^* \quad (32)$$

where $k_B$ is the Boltzmann constant ($1.3807 \times 10^{-23} \text{ J K}^{-1}$) and $h$ is the Planck constant ($6.626 \times 10^{-34} \text{ J s}$).
Table 3 Thermokinetic parameters for thermal decomposition process of HNIW/TNT cocrystal for $G(a) = [1 - \ln(1 - a)]^{2/3}$, $f(\alpha) = \frac{3}{2} (1 - \alpha)^{-1} \ln(1 - \alpha)$

| Method                           | $\beta$/K min$^{-1}$ | $E$/kJ mol$^{-1}$ | $\lg(A_0$/s$^{-1}$) | $r$   | $Q$   |
|---------------------------------|----------------------|-------------------|----------------------|-------|-------|
| Ordinary-integral equation$^{30}$| 2.5                  | 231.87            | 22.69                | 0.9998| 0.0028|
|                                 | 5.0                  | 238.46            | 23.37                | 0.9998| 0.0045|
|                                 | 10.0                 | 236.01            | 23.13                | 0.9991| 0.0162|
|                                 | 15.0                 | 233.85            | 22.87                | 0.9986| 0.0256|
|                                 | 20.0                 | 234.05            | 22.83                | 0.9982| 0.0336|
| Universal integral method$^{31}$| 2.5                  | 235.87            | 21.35                | 0.9998| 0.0043|
|                                 | 5.0                  | 242.52            | 22.02                | 0.9998| 0.0045|
|                                 | 10.0                 | 240.20            | 21.79                | 0.9992| 0.0161|
|                                 | 15.0                 | 237.98            | 21.53                | 0.9987| 0.0255|
|                                 | 20.0                 | 238.21            | 21.50                | 0.9983| 0.0335|
| MacCall–Tanner$^{32}$           | 2.5                  | 232.93            | 22.80                | 0.9998| 0.0008|
|                                 | 5.0                  | 239.68            | 23.50                | 0.9998| 0.0008|
|                                 | 10.0                 | 238.68            | 23.49                | 0.9998| 0.0008|
|                                 | 15.0                 | 235.19            | 23.01                | 0.9987| 0.0048|
|                                 | 20.0                 | 235.45            | 22.98                | 0.9983| 0.0063|
| Satava–Sestak equation$^{33}$   | 2.5                  | 228.11            | 22.34                | 0.9998| 0.0008|
|                                 | 5.0                  | 234.48            | 23.00                | 0.9998| 0.0008|
|                                 | 10.0                 | 237.39            | 23.26                | 0.9992| 0.0030|
|                                 | 15.0                 | 230.24            | 22.54                | 0.9987| 0.0048|
|                                 | 20.0                 | 230.49            | 22.51                | 0.9983| 0.0063|
| Agrawal$^{34}$                  | 2.5                  | 231.87            | 22.69                | 0.9998| 0.0043|
|                                 | 5.0                  | 238.46            | 23.36                | 0.9998| 0.0045|
|                                 | 10.0                 | 236.10            | 23.13                | 0.9991| 0.0162|
|                                 | 15.0                 | 233.85            | 22.87                | 0.9986| 0.0256|
|                                 | 20.0                 | 234.05            | 22.83                | 0.9982| 0.0336|
| Mean                            |                      | 235.44            | 22.70                |       |       |
| Kissinger$^{27}$                |                      | 239.40            | 23.50                | 0.9969|       |
| Flynn–Wall Ozawa$^{28}$         |                      | 235.45            |                     | 0.9971|       |

$^a$ $\beta$ is the heating rate; $E$ is the activation energy; $A_0$ is the pre-exponential constant; $r$ is the linear correlation coefficient; $Q$ is the variance.

### 3.11 The determination of the adiabatic time-to-explosion

The adiabatic time-to-explosion ($t_{\text{adi}}$, s) of energetic materials is the time of energetic material thermal decomposition transitioning to explosion under adiabatic conditions, and it is an important parameter for assessing the thermal stability and the safety of energetic materials. The estimation formulae used to calculate the adiabatic time-to-explosion ($t$) of energetic materials are Smith’s eqn (33)-(35) taken from ref. 36.

$$\frac{C_p}{Q} \int_{T_0}^{T} \frac{C_p}{Q} \exp\left(-\frac{E}{RT}\right) f(\alpha) \, dT$$

$$\alpha = \int_{T_0}^{T} \frac{C_p}{Q} \, dT$$

$$t = \frac{1}{QA} \int_{T_0}^{T} \frac{C_p}{Q} \exp\left(-\frac{E}{RT}\right) f(\alpha) \, dT$$

where $C_p$ is the specific heat capacity (J g$^{-1}$ K$^{-1}$); $f(\alpha)$ is the differential mechanism function; $E$ is the apparent activation energy; $A$ is the pre-exponential constant; $Q$ is the heat of decomposition; $R$ is the gas constant (8.314 J mol$^{-1}$ K$^{-1}$); and $\alpha$ is the conversion degree.

By substituting the original data of $C_p = 1.01$ J g$^{-1}$ K$^{-1}$, $f(\alpha) = (1 - \alpha)^{-1} \ln(1 - \alpha)$, $E = 239$ 400 J mol$^{-1}$, $A = 10^{13.50}$ s$^{-1}$, $Q_d = 3092.36$ J g$^{-1}$, and $R = 8.314$ J mol$^{-1}$ K$^{-1}$, the integral upper limit $T = T_b = 472.82$ K and the lower limit $T_0 = T_{00} = 464.45$ K into eqn (35), the values of $t$ of 4.40 s for $n = 0$, 4.42 s for $n = 1$, and 4.43 s for $n = 2$ are obtained.

### 3.12 The critical temperature of hot-spot initiation ($T_{cr}$)

The interior of energetic materials (EMs) could create a local thermal point when the EMs accept energy, and the EMs will explode from thermal decomposition when the hot-spot temperature reaches the explosive temperature. The critical temperature of hot-spot initiation ($T_{cr}$) is an important parameter for evaluating the thermal safety of EMs.

By submitting the density $\rho = 1.844$ g cm$^{-3}$ of HNIW/TNT cocrystal, specific heat capacity $C_p = 1.01$ J g$^{-1}$ K$^{-1}$, thermal conductivity $\lambda = 16.8 \times 10^{-4}$ J cm$^{-1}$ K$^{-1}$, heat of decomposition $Q_d = 3092.36$ J g$^{-1}$, kinetic parameters $E = 239$ 400 J mol$^{-1}$ and $A = 10^{13.50}$ s$^{-1}$, $T_{\text{room}} = 293.15$ K, $R = 8.314$ J mol$^{-1}$ K$^{-1}$, hot-spot critical radius $a = 10^{-3}$ cm (ref. 36) and time interval $t - t_0 = 10^{-4}$ s (ref. 37) to Bruckman–Guillet’s first-order estimation equation [eqn (36)],$^{38,39}$ the value of $T_{cr,\text{ hotspot}}$ of 258.75 °C (531.90 K) is obtained.
3.13 50% drop height (H_{50}) impact sensitivity

Impact sensitivity is an important parameter for evaluating the security and reliability of EMs and can be characterized by 50% drop height (H_{50}). Using data of \( \lambda = 16.80 \times 10^{-4} \text{ J cm}^{-1} \text{ s}^{-1} \) K^{-1}, \( \rho = 1.844 \text{ g cm}^{-3}, Q_d = 3146.89 \text{ J g}^{-1}, E = 239 \text{ 400 J mol}^{-1} \), and \( A = 10^{23.50} \text{ s}^{-1} \), the \( H_{50} \) of HNIW/TNT cocrystal was estimated as 19.46 cm by Friedman's formula (eqn (37)). This value shows that it has impact sensitivity level approaching those of PETN (15.6 cm) and tetryl (17.6 cm)\(^{17}\)

\[
0.282312 \log(H_{50}) + \log\left(\frac{\lambda}{A \rho Q_d}\right) - 0.347174 + \frac{0.02612E}{T_1 + 33.8765H_{50}^{0.864025}} = 0
\]  

(37)

3.14 Critical thermal explosion ambient temperature \( T_{acr} \), thermal sensitivity probability density function \( S(T) \), safety degree SD and thermal explosion probability \( P_{TE} \)

To explore the heat resistance of HNIW/TNT cocrystal, the values of \( T_{acr}, S(T) \) vs. \( T \) relation, SD and \( P_{TE} \) are calculated by Frank-Kamenetskii (38)\(^{4a}\) and Wang–Du’s formulas (39)–(42)\(^{41}\).

In formulas (38)-(44), \( T_{acr} \) is the critical thermal explosion ambient temperature in K; \( E \) is the activation energy in J mol\(^{-1}\); \( A \) is the pre-exponential constant in s\(^{-1}\); \( R \) is the gas constant in 8.314 J K\(^{-1}\) mol\(^{-1}\); \( \lambda \) is the thermal conductivity in W m\(^{-1}\) K\(^{-1}\); \( \delta \) is the Frank-Kamenetskii parameter (FK); \( \delta_{cr} \) is the criticality of thermal explosion of exothermic system; \( r \) is characteristic measurement of reactant in m; \( Q_d \) is decomposition heat in J kg\(^{-1}\); \( \rho \) is density in kg m\(^{-3}\); \( \mu_T \) is the average value of temperature; \( \sigma_r \) is the standard deviation of FK parameter; \( \sigma_{cr} \) is the standard deviation of ambient temperature; \( T \) is surrounding temperature; \( S(T) \) is the thermal sensitivity probability density function; SD is safety degree; and \( P_{TE} \) is thermal explosion probability.

\[
T_{acr} = \frac{-E_K}{2R \text{ Lambert } W_{-1} \sqrt{\frac{\lambda E_K \delta_{cr}}{r^2 Q_d \rho A_K R}}}
\]  

(38)

\[
S(T) = \frac{W(E_K - 2RT)}{2\pi \sigma_r^2 RT^4} \times \exp\left\{-\frac{\exp\left(\frac{E_K}{RT}\right) - \delta_{cr}}{2\sigma_r^2 - \frac{E_K}{RT}}\right\}^2
\]  

(39)

where:

\[
\delta_{cr} = \frac{E_K}{2R \text{ Lambert } W_{-1} \left( \frac{1}{2} \sqrt{\frac{\lambda E_K \delta_{cr}}{r^2 Q_d \rho A_K R}} \right)}
\]  

(40)

\[
\sigma_r = W\left(\frac{E_K - 2R \mu_T}{R \mu_T^4}\right) \exp\left(-\frac{E_K}{R \mu_T} \sigma_T\right)
\]  

(41)

\[
\mu_T = \frac{-E_K}{2R \text{ Lambert } W_{-1} \left( \frac{1}{2} \sqrt{\frac{\lambda E_K \delta_{cr}}{r^2 Q_d \rho A_K R}} \right)}
\]  

(42)

and \( \sigma_r \) is the standard derivation of the Frank-Kamenetskii parameter, \( \sigma_T \) is the standard derivation of the measured surrounding temperature, and \( \mu_T \) is the mean value of \( T \).

SD was obtained by eqn (43):

\[
SD = \int_0^{T_{cr}} \int_0^{T_{cr}} W(E_K - 2RT) \frac{2\pi \sigma_r^2 \sigma_T^2 RT^4}{2\pi \sigma_r^2 RT^4} \exp
\]  

(43)

\[
\left\{-\frac{\exp\left(\frac{E_K}{RT}\right) - \delta_{cr}}{2\sigma_r^2 - \frac{E_K}{RT}}\right\}^2
\]  

The thermal explosion probability (\( P_{TE} \)) is expressed as eqn (44):

\[
P_{TE} = 1 - SD
\]  

(44)

![Fig 3 The S(T) vs. T relation curves for infinite flat like, infinite cylindrical and spherical HNIW/TNT cocrystal.](image)
4 Conclusions

[1] The thermodynamic data describing the energetic characteristics of HNIW/TNT cocrystal are presented: (a) \( \Delta f_m^\circ \) (HNIW/TNT cocrystal, s, 298.15 K) = \(-7012.14 \pm 3.42\) kJ mol\(^{-1}\); (b) \( \Delta U \) (HNIW/TNT cocrystal, s, 298.15 K) = \(-7023.91 \pm 3.40\) kJ mol\(^{-1}\); (c) chemical energy of detonation \( Q \) = 6184.71 J g\(^{-1}\).

[2] The nonisothermal thermal safety data used to evaluate the heat resistance and the transition resistance from thermal decomposition to thermal explosion of small-scale HNIW/TNT cocrystal and the thermal safety of HNIW/TNT cocrystal (Fig. 3) and thermal sensitivity of the HNIW/TNT cocrystal (Table 4) are obtained, showing that the accelerating tendency from adiabatic decomposition to explosion of large-scale HNIW/TNT cocrystal and the thermal safety of HNIW/TNT cocrystal with different shapes decreases in the order: sphere > infinite cylinder > infinite flat.

### Table 4 Results for the determination of thermal sensitivity for the HNIW/TNT cocrystal

| Shape types of reactant | \( W/\text{K}^2 \) | \( T_{av}/\text{K} \) | \( \sigma_1/\text{K} \) | \( T_{S(T)\text{max}}/\text{K} \) | \( S(\sigma)_{\text{TP}} \) | \( \text{SD}/\% \) | \( \text{P}_{\text{TE}}/\% \) |
|-------------------------|------------------|-----------------|----------------|----------------|----------------|----------------|----------------|
| 1                       | 3.091 \times 10^{12} | 469.69 | 4.19 | 470.58 | 0.0581 | 78.57 | 21.43 |
| 2                       | 3.091 \times 10^{12} | 465.70 | 2.57 | 470.58 | 0.0581 | 78.17 | 21.83 |
| 3                       | 3.091 \times 10^{12} | 459.39 | 1.16 | 464.26 | 0.0581 | 77.54 | 22.46 |

\( * \) 1 is the sphere; 2 is the infinite cylinder; 3 is the infinite flat.

### Conflicts of interest

There are no conflicts to declare.

### Acknowledgements

We gratefully acknowledge the financial support from the National Natural Science Foundation of China (Grant No. 21673182, and 21703168).

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By substituting the values of \( r = 1 \text{ m} \), \( Q_a = 3.09236 \times 10^6 \text{ J kg}^{-1} \), \( E = 239\ 400 \text{ J mol}^{-1} \), \( A = 10^{23.50} \text{ s}^{-1} \), \( \rho = 1.844 \times 10^3 \text{ kg m}^{-3} \), \( \lambda = 0.168 \text{ W m}^{-1} \text{ K}^{-1} \), ambient temperature \( T_a = 400 \text{ K} \), \( \sigma_0 = 10 \text{ K into eqn } (39)-(42) \), the \( S(T) \) vs. \( T \) relation curves for infinite flat, infinite cylindrical and spheroid HNIW/TNT cocrystal (Fig. 3) and thermal sensitivity of the HNIW/TNT cocrystal (Table 4) are obtained, showing that the accelerating tendency from adiabatic decomposition to explosion of large-scale HNIW/TNT cocrystal and the thermal safety of HNIW/TNT cocrystal with different shapes decreases in the order: sphere > infinite cylinder > infinite flat.
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