Constraints on cosmic ray propagation from radio continuum data of NGC 2146

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ABSTRACT
We present high-sensitivity multi-frequency radio continuum observations of the starburst galaxy NGC 2146. We have fitted these data with a three-dimensional diffusion model. The model can describe the radio emission from the inner disc of NGC 2146 well, indicating that diffusion is the dominant mode of propagation in this region. Our results indicate that NGC 2146 has recently undergone a starburst, the star forming activity being located in a central bar. The spatial variations of the radio emission and of the spectral index yield tight constraints on the diffusion coefficient $D_0$ and the energy dependence of the diffusion. Away from the central bar of the galaxy the radio emission becomes filamentary and the diffusion model is found to be a poor fit to the data in these regions; we attribute this to different transport processes being important in the halo of the galaxy.

Key words: diffusion - cosmic rays - galaxies: individual: NGC 2146 - radio continuum: galaxies.

1 INTRODUCTION
Multi-frequency radio observations of nearby, face-on galaxies present a unique way to study the cosmic ray (CR) propagation within their discs. These studies provide constraints on the main parameters of this propagation, i.e. the value and energy dependence of the diffusion coefficient and the form of the electron energy distribution immediately after acceleration. Furthermore, because of the relatively long radiative life-time to several $10^7$ yr) such observations also provide information about the temporal evolution of the sources of the CRs on the same time-scale; in turn, since the sites of acceleration are supernova remnants the data are probing the history of star formation on time-scales up to of order $10^9$ yr.

To date, the parameters describing CR propagation have been derived only for our Galaxy; radio observations are the only way of obtaining information for external galaxies. In this paper we analyse high-sensitivity multi-frequency radio data for the nearby galaxy NGC 2146. Our data have sufficient frequency coverage that we can include in our model fits both a thermal and a diffuse synchrotron component for the radio emission.

NGC 2146 is a very luminous radio source ($P_{\text{rad,1.5 GHz}} = 5.9 \times 10^{22}$ W Hz$^{-1}$) at a distance of 21.8 Mpc (Benvenuti, Capacioli & D’Odorico 1975, adjusted to $H_0=50$ km s$^{-1}$ Mpc).

Most of its radio luminosity is due to a compact starburst in its centre. The extent of the radio emission (1.5 arcmin $\approx 9.6$ kpc) is much less than the extent of the optical emission ($\approx 6$ arcmin). This suggests that active star formation (both current and in the recent past) is confined to this central region of NGC 2146. In this paper we are discussing only this inner region of the galaxy ($\approx 1.5 \times 0.7$ arcmin$^2$) which is characterized by the strong radio emission. Optical images of NGC 2146 show it to be a peculiar spiral galaxy (e.g. Benvenuti et al. 1975). Hutchings et al. (1990) have presented a detailed study of NGC 2146 in several wavebands and proposed that the galaxy is in the late stages of a merger which has given rise to an intense burst of star formation in the nucleus.

2 OBSERVATIONS
NGC 2146 was observed with the VLA at 1.5 GHz, 8.4 GHz and 327 MHz, and with the Cambridge 5-km Ryle Telescope (RT) at 5 and 15 GHz. Additionally, existing VLA data (C array) at 1.5 GHz (Condon 1983) were available. When the observations of NGC 2146 were made, the RT was operated with a band-width of 280 MHz split into 28 10-MHz frequency channels; together with the minimum baseline of 18 m this provides excellent temperature sensitivity at both 5 and 15 GHz.

For the RT observations a total of five telescope configurations at each observing frequency were employed giving a
nearly fully filled aperture out to the maximum baseline. A minimum of two 12-h runs in each configuration were obtained; any data of poor quality were rejected. This gave a resolution of approximately $1.0 \times 1.0 \text{cosec}(\delta)$ arcsec$^2$ at 15 GHz and $3.0 \times 3.0 \text{cosec}(\delta)$ arcsec$^2$ at 5 GHz. At 5 GHz observations of phase calibrators were made at the beginning and end of each run, while at 15 GHz calibration observations were interleaved with those of NGC 2146. 3C 286 and 3C 48 were observed regularly as flux calibrators. Calibration and data-editing (principally to remove narrow-band and time-varying
interference) were performed in the MRAO package POSTMORTEM, with subsequent reduction in AIPS and the MRAO package ANMAP.

The 8.4-GHz VLA observations were in the B, C and D arrays with the 1.5-GHz observations in B array and the 327-MHz observations in A array only; the observations were performed during 1990/91. Reduction of the data followed standard VLA procedures with calibration, editing and imaging performed in AIPS.

A number of maps were made at each frequency by tapering the aperture plane to highlight structure on different angular scales. For the spectral comparison we used only the four highest frequencies and all the maps were made with very similar aperture plane coverage, CLEANed and restored (or convolved in the case of the 1.49-GHz image) to a common resolution of 4.7 × 4.7 arcsec². All maps have been corrected for the primary beam response of the telescope used to make the observations. This set of four images is shown in Fig. 1, together with a high-resolution image at 15 GHz in Fig. 2 and the 327-MHz image in Fig. 3. In Fig. 4 a map of the spectral index between 1.5 and 8.4 GHz is shown.

3 RADIO PROPERTIES OF NGC 2146

Most of the radio emission of NGC 2146 lies along an elongated, bar-like structure in position angle 143° ± 3° coincident with the optical major axis (143°, Benvenuti et al. 1975). This elongated shape could be a disc viewed from a high inclination or it could be due to a real bar-like shape of the sources of the CRs. From the radio data at one frequency alone it is not possible to distinguish between these two cases. However, as will be shown in the following, the variations of the radio spectral index together with a model for the CR propagation allow us to draw conclusions about the shape of the CR sources. In the high-resolution image (Fig. 2), the sources at 15 GHz show a distinctive S shape which had already been noticed in earlier observations by Kronberg & Biermann (1981). The central region is shown in our highest resolution images to contain a number of luminous unresolved sources superimposed on the general background emission.

At higher frequencies NGC 2146 appears more compact and shows relatively little emission away from the major axis of the radio emission, while at lower frequencies the emission has an irregular appearance and several extensions perpendicular
to the major axis which are prominent particularly in the 1.5-GHz and the 327-MHz images.

4 MODELLING THE RADIO EMISSION

Our aim in this work is to explain the multi-frequency radio data by a combination of thermal emission and non-thermal electrons produced on average per energy interval by a SNR.

(iii) The spatial distribution of a source is approximated by an ellipsoid, Gaussian distribution:

\[
\mathcal{A}(r) = \pi^{-\frac{1}{2}}(R_x R_y R_z)^{-\frac{1}{2}} \times \exp \left\{ -\left( \frac{(x-x_0)^2}{R_x^2} + \frac{(y-y_0)^2}{R_y^2} + \frac{(z-z_0)^2}{R_z^2} \right) \right\} \]

with \((x_0, y_0, z_0)\) indicating the site of the centre of the source and \(R_x R_y R_z\) the axes of the ellipsoid. In the following, we will identify the major axes of NGC 2146 with the \(x\)-axis, the direction within the galactic plane perpendicular to the major axis with the \(y\)-axis and the direction perpendicular to the plane with the \(z\)-axis.

Equation (1) can be solved for an infinite space following the analysis of Syrovatskii (1959). In a steady-state situation (i.e. for constant sources) the electron distribution function is given by

\[
f(E, r) = \frac{q_{SN}}{v_{SN}} \sum_i \int_{E_i}^{E_f} \frac{dE_0}{E_0} \left( \frac{E_0}{m_e c^2} \right)^{-\gamma} \exp \left\{ -\left( \frac{(x-x_0)^2}{4R_x^2} + \frac{(y-y_0)^2}{4R_y^2} + \frac{(z-z_0)^2}{4R_z^2} \right) \right\} \]

where \(E_x\) and \(E_1\) are the upper and lower ends of the range of electron injection energies and \(\lambda\) is given by

\[
\lambda(E, E_0) = \int_E^{E_0} \frac{D(E')}{b(E')} dE' = \frac{1}{C(1-\mu)} D_0 \left( E_n - E_0 \right).
\]

If temporal changes are important, a similar solution for \(f(E, r, t)\) can be derived. The synchrotron emission \(P_{\text{syn}}(v, r, t)\) is derived from \(f(E, r, t)\) with the simplifying assumption that each electron emits its synchrotron radiation at the maximum frequency of the synchrotron spectrum:

\[
P_{\text{syn}}(v, r, t) = f(E(v), r, t) \frac{dE}{dr} \frac{dv}{dE} \]

with the emitting frequency being

\[
v = \left( \frac{E}{m_e c^2} \right) v_0
\]

where \(v_0 = eB/m_e c^2\) is the gyrofrequency.

The thermal emission is also described as arising from ellipsoidal sources, which are not necessarily the same as the CR sources:

\[
P_{\text{therm}}(v, r) \propto \sum_i \mathcal{A}(r) v^{-0.1}.
\]

Both \(P_{\text{syn}}\) and \(P_{\text{therm}}\) have to be integrated through the halo along the line of sight, taking into account the inclination angle of the galaxy, and convolved with the beam. The total radio emission, \(P_{\text{rad}}\), is finally obtained as the sum of \(P_{\text{syn}}\) and \(P_{\text{therm}}\).
5 FITTING THE MODEL TO THE RADIO DATA

In order to keep the diffusion model as simple as possible we shall assume a steady state, i.e. we attempt to fit a model in which the star formation rate and hence the sources of thermal and non-thermal emission do not show any temporal variations. In NGC 2146 the estimated life-time of CR electrons is, due to the high radiation losses (see below), extremely short (less than 2 x 10^6 yr). On these short time-scales the assumption of a steady state seems reasonable. Furthermore we will assume as the simplest case that H II regions and supernova remnants are co-spatial (at least at the resolution of our radio images). This will be a good approximation if the sites of star formation have not changed during the past ≈ 10^8 yr, i.e. the life-time of supernova progenitors (M ≥ 5 M⊙). If there has been significant propagation of the star formation process through the galaxy then this assumption must be modified.

Additionally we can constrain some of the parameters directly from observational data.

(i) The inclination of NGC 2146 is θ = 65° (Benvenuti et al. 1975). Due to the disturbed appearance of NGC 2146 the inclination angle is unlikely to be precisely determined; we shall adopt this value and discuss this point more fully in Section 6.1. The radius of the CR sources perpendicular to the disc is taken to be R⊙ = 100 pc, which is a typical scale height of the molecular gas disc (e.g. Unsöld & Baschek 1991) in which we expect massive star formation to be located.

(ii) We estimate the magnetic field B by applying a minimum energy calculation. We adopt standard values for most parameters: a frequency range of 10^7 - 10^10 GHz; a radio spectral index α = 0.7 (here and in the following we define the spectral index α as Fν ∝ ν^{-α}); a ratio of total energy of CRs to total energy of electrons k = 100. For measured quantities we use the emission at 1.5 GHz. We obtain the volume of the emitting region at this frequency by assuming that it can be approximated by a cylinder with a height of 1 kpc and a radius of 45 arcsec (≈ 5 kpc) which corresponds to the lowest contour of the 1.5-GHz image. With these assumptions we obtain B = 38 μG.

(iii) The energy density of the radiation field, U_{rad}, can be calculated from the bolometric luminosity:

\[ U_{rad} = \frac{2L_{bol}}{cπR^2} = \frac{4\pi c(\text{bol}/W)}{R_{kpc}} \times 1.4 \times 10^{-35} \left[ \frac{\text{eV}}{\text{cm}^2} \right]. \]  

For NGC 2146 the greatest part of the luminosity is emitted in the far-infrared (FIR); we therefore approximate the bolometric luminosity L_{bol} by the far-infrared luminosity L_{FIR}. For the radius R we take the radius derived from our radio data (R = 5 kpc) as this will correspond to the region in which most star formation is currently occurring. With these assumptions we obtain \( U_{rad} = 20 \text{ eV cm}^{-3} \).

With these derived values, the fitted values of the diffusion model now proceed by fitting to slices extracted from our multi-frequency radio images along both the major and minor axes of NGC 2146. In Figs 5 and 6 we show the observational data and the corresponding model fits.

In constraining the parameters for the model we note some general features of the data.

(i) The spectral index between 1.5 and 8.4 GHz is approximately constant along the major axis (Fig. 7a); this suggests that the CR source is itself extended in this direction unless the diffusion coefficient had a strong energy dependence with \( \mu \approx 1 \). In this latter case \( \alpha \) (equation 8) would be largely independent of the electron energy and hence the spatial distribution of the electrons would also be energy independent (see equation 7).

(ii) The steepening of the spectrum away from the major axis (Fig. 7) indicates that \( \mu \) is considerably less than one and that the electrons must have suffered from energy losses.

(iii) The radio flux decreases away from the centre of the galaxy along both the major and minor axes (Figs 5 and 6).

Taken together, these observations suggest that the model should have the following general characteristics.

(1) The source distribution is extended along the major axis but not along the minor axis, i.e. it has the shape of a bar.

(2) The energy dependence of the diffusion coefficient, \( \mu \), must be considerably less than unity, and is constrained by the data along the minor axis of NGC 2146.

The fitting of the model to the observational data now proceeds by a straightforward search of parameter space for model parameters that lead to the best fit of the multi-frequency radio data. The model most strongly constrains the spatial distribution and strength of the thermal and non-thermal emission regions, and also the energy dependence of the diffusion coefficient. Our results and conclusions for the simplest form of the model without temporal variations are shown in Fig. 5 and can be summarized as follows.

(1) The source structure cannot be adequately represented by a single ellipsoidal emission region. Two sources, both centred at the maximum of the radio emission, are necessary to account for the data. Our best-fitting parameters for these two sources are

source 1: \( R_{x,1} = 1.3 \text{ kpc}, R_{y,1} = 0.7 \text{ kpc}, \text{ relative intensity} 1; \)

source 2: \( R_{x,2} = 3.0 \text{ kpc}, R_{y,2} = 0.5 \text{ kpc}, \text{ relative intensity} 0.3. \)

We interpret this result as suggesting that the distribution of CR sources and hence star formation activity is in the form of a bar. The parameters describing source 1 are relatively well constrained by the shape of the radio emission (for a fixed value of the galaxy inclination). The parameters of source 2 are less well constrained; however, this has a relatively minor effect on the other model parameters.

(2) The injection index of the electron population is \( \gamma = 1.7 \) and we infer a lower thermal fraction of \( P_{\text{therm}}/P_{\text{rad}} = 17 \) per cent at 15 GHz. The thermal fraction is constrained by the radio spectrum at the centre of the galaxy.

(3) It is clear from Fig. 5 that we are not able, with the simplest form of the model, to get good fits to the data over the whole frequency range: at 5, 8.4 and 15 GHz the model predictions for the peak radio emission are either slightly too low or too high. The discrepancies, however, never exceed 10 per cent and it should furthermore be noted that the shape of the radio emission can be reproduced well at all frequencies.

The results obtained by allowing for temporal variations in the star formation rate, while keeping the source distribution constant, are shown in Fig. 6. In this case, an injection index of \( \gamma = 1.65 \) is used and the temporal variations are assumed to have a simple form with injection of CR electrons.
having stopped $5.7 \times 10^5$ yr ago. The predicted thermal contribution is now much greater than in the steady-state model. At 15 GHz the emission is almost completely thermal and at 1.5 GHz the thermal fraction is still $P_{\text{therm}}/P_{\text{rad}} = 27$ per cent. The time-dependent solution produces an improved model fit as it permits an aged electron population to develop. In general, for both the steady-state and time-dependent cases, the fits along the major axis are worse than those along the minor axis —

this is because of the structure of $P_{\text{rad}}$ which reflects the complicated intrinsic source structure (see Fig. 2) which we have not taken into account. However, this does not significantly affect our conclusions concerning propagation of CRs to be discussed below.

(4) The value of the diffusion coefficient $D_0$, and its energy dependence, is strongly constrained by the data perpendicular to the inferred bar within NGC 2146 along the minor axis.

Figure 5. Slices of the radio emission at 1.5, 5 and 8.4, 15 GHz along the minor and the major axes (full lines), together with the best-fitting steady-state model results (dashed lines). The parameters are: $\gamma = 1.7, \mu = 0, D_0 = 2 \times 10^{28}$ cm$^2$ s$^{-1}$, $P_{\text{therm}}$(1.5 GHz) = 4 mJy beam$^{-1}$ at $r = 0$, $R_{x,1} = 1.3$ kpc, $R_{y,1} = 0.7$ kpc, $R_{x,2} = 3.0$ kpc, $R_{y,2} = 0.5$ kpc.
Figure 6. Slices of the radio emission (full lines), together with the best-fitting results for a model with temporal changes in the injection rate (dashed lines). The parameters are: $y = 1.65$, $\mu = 0$, $D_0 = 2 \times 10^{28}$ cm$^2$ s$^{-1}$, $P_{\text{therm}}(1.5 \text{ GHz}) = 23$ mJy beam$^{-1}$ at $r = 0$; the source structure is the same as in Fig. 5. The injection of CRs stopped $5.7 \times 10^5$ yr ago.

Furthermore, the results are very similar for both the steady-state model and a time-dependent model. In Fig. 8 we show the results for the steady-state case - the best fit for the diffusion coefficient is $D_0 = 1.0$ to $4.0 \times 10^{28}$ cm$^2$ s$^{-1}$, with $\mu = 0$. The shape of the spectral index distribution along the minor axis depends sensitively on $\mu$, which is illustrated in Fig. 7. Our best estimate for $\mu$ is in the range $0.0$ to $0.2$ with a firm upper limit of $\mu < 0.5$.

6 DISCUSSION

6.1 Model uncertainties

As illustrated in Figs 5-8, the model describes the data well and allows us to constrain important parameters such as the diffusion coefficient and its energy dependence and infer the existence of a central bar. The error in the determination of these parameters depends, however, not only on the quality...
The source distribution is parametrized as in Fig. 5. The results for different values of \( \mu \). The parameters are: \( \mu \). The parameters are as in Fig. 5.

The time-scale of the changes implied by the data is rather short, less than \( 10^6 \) yr; however, there is a strong dependence on \( B \) and \( U_{\text{rad}} \). Whereas our estimate for \( U_{\text{rad}} \): \( t \sim B^{1/2}/(U_{\text{rad}} + U_B) \). Whereas our estimate for \( U_{\text{rad}} \) does not suffer from large uncertainties, \( B \) is very uncer-
tain and an improved estimate would require an independent determination of the magnetic field.

The main sources of error for the diffusion coefficient, $D_0$, are the uncertainty in $U_{rad}$, $B$, the distance to NGC 2146 and the assumed structure of the emitting region. In principle it could be possible to increase/decrease the size of the CR source along the minor axis ($R_m$) and try to fit the data by decreasing/increasing $D_0$. If $R_m$ is very small, even with a large value of $D_0$ the model cannot produce the observed shape of $P_{rad}$. On the other hand, a larger assumed source size would make it impossible to fit the spectral variations unless we assumed that the injection index of the CR population varied within the disc of the galaxy, and/or that different regions of the galaxy had undergone very different star formation histories. Within the range of acceptable $R_m$ the estimated values for $D_0$ all lie within our quoted error bounds. The uncertainty in the inclination angle of NGC 2146 does not affect our estimates of $D_0$ and $\mu$ greatly and it most strongly affects the assumed source size. Our conclusion regarding the bar-like shape of the star forming region therefore depends sensitively on the assumed inclination angle. However, only for a severe underestimate of the true inclination angle of NGC 2146 (i.e. if $i \gtrsim 80^\circ$) can this conclusion not be maintained. In this case the radio emission along the minor axis would be almost entirely from the halo.

6.2 CR propagation in the central disc and halo

The diffusion model is a good fit to the radio data for NGC 2146 along the major axis of the galaxy and along the minor axis for distances less than 10 arcsec (2.6 kpc) from the major axis. This suggests that diffusion is the dominant mode of propagation in this region which corresponds to the inner, most actively star forming disc of NGC 2146.

At distances greater than 10 arcsec from the centre of the galaxy along the minor axis the model is no longer an adequate fit to the data (Figs 5 and 6). The shape of the 1.5-GHz emissivity is very flat, suggesting that transport of CR electrons is more efficient than would be expected from diffusion alone. Furthermore, the spectral index flattens which indicates that (i) the energy losses have decreased rapidly, or (ii) the diffusion coefficient increases, or (iii) a much faster process than diffusion is responsible for the transport of the CR electrons. Upon examination of the radio emission in the region where the diffusion model begins to fail, we note that the radio images (Figs 1 and 3) show filamentary structure. The most likely reason for this behaviour is that away from the centre of the galaxy a large fraction of the radio emission is from a halo which is seen in projection.

The propagation of CR electrons in the halo might be more complicated than we have considered for the propagation within the disc. Evidence for this comes from observations of the edge-on galaxies NGC 891 and NGC 4631 where extended radio continuum emission in the halo with a rather flat spectral index has been observed (Hummel 1991). Breitschwerdt (1994) has explained this flat spectral index in a galactic wind model including diffusive and convective transport of CRs. Siemionce & Cesarsky (1991) modelled the spectral index in the halo of NGC 891 by a diffusion model with an outwardly increasing diffusion coefficient. Both galaxies show that in the halo the propagation of CR electrons is faster than that predicted by steady-state diffusion alone.

Due to the strong star formation activity in NGC 2146, an outflow from the disc triggered by correlated SN explosions may be present, a mechanism which is variously described as a 'galactic fountain' (Shapiro & Field 1976) or 'chimney' model (Ikeuchi 1988; Norman & Ikeuchi 1989). Such an outflow would transport CRs and magnetic field into the halo and could therefore account for a higher radio emission in the halo than expected from a pure diffusion model. The analysis of X-ray and optical data of NGC 2146 (Armus et al. 1995) has shown that there are indeed indications of the existence of such a starburst-driven superwind.

6.3 Star formation in NGC 2146

Hutchings et al. (1990) proposed that NGC 2146 is in the late stage of a merger. The merger must have begun $\gtrsim 10^9$ yr ago as the rotation curve does not appear to be disrupted in the outer regions of the galaxy (Young et al. 1988a show the outer regions of the galaxy to have non-circular motions of the order of 100 km s$^{-1}$). In this scenario material has collapsed into the centre of the galaxy and a starburst has commenced in the nucleus.

The data and model presented in this paper further emphasize that active star formation is confined only to the centre of the galaxy. The radio images show that the star formation activity is located in a peculiar spiral S shape around the peak of the radio emission. The merger may have triggered the formation of a bar which feeds the nuclear starburst with material and is responsible for the unusual structure of the radio emission. Star formation is proceeding all along the central bar, and the nucleus is not prominent in the high-resolution radio images. Young et al. (1988a) suggest that, if the galaxy is in the late stage of a merger, the nucleus of the merging companion could be obscured by the dust lane. The images of the radio emission presented here argue against this, as we do not find two spatially distinct peaks of radio emission which could be identified as the nuclei of the merging systems. Instead, the star formation is distributed throughout the bar-like central region. The unresolved sources seen on our highest resolution images have sizes of less than 100 pc and may represent isolated pockets of star formation or could be individual high-luminosity supernovae as seen in M82 (Muxlow et al. 1994). The presence of dynamical features such as the arm in the H$\alpha$ emission (Young, Kleinmann & Allen 1988b) and the bar in the radio emission suggest that this starburst is dynamically driven, i.e. due to a merger or an interaction.

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REFERENCES

Armus L, Heckman T.M., Weaver K.A., Lehnert M.D., 1995, ApJ, 445, 666
Benvenuti P, Capacioli M., D’Odorico S., 1975, A&A, 41, 91
