A discontinuous control volume finite element method for multi-phase flow in heterogeneous porous media

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\textbf{A B S T R A C T}

We present a new, high-order, control-volume-finite-element (CVFE) method for multi-phase porous media flow with discontinuous 1st-order representation for pressure and discontinuous 2nd-order representation for velocity. The method has been implemented using unstructured tetrahedral meshes to discretize space. The method locally and globally conserves mass. However, unlike conventional CVF formulations, the method presented here does not require the use of control volumes (CVs) that span the boundaries between domains with differing material properties. We demonstrate that the approach accurately preserves discontinuous saturation changes caused by permeability variations across such boundaries, allowing efficient simulation of flow in highly heterogeneous models. Moreover, accurate solutions are obtained at significantly lower computational cost than using conventional CVFE methods. We resolve a long-standing problem associated with the use of classical CVFE methods to model flow in highly heterogeneous porous media.

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1. Introduction

Many geologic porous media are highly heterogeneous: they contain domains of contrasting material properties such as porosity, permeability and capillary pressure. Moreover, these domains often have complex three-dimensional (3D) geometries and spatial distribution, and the changes in material properties across the domain boundaries are effectively discontinuous, because they occur over a few tens or hundreds of grains (e.g. [24], [12], [44], [38], [27], Fig. 1).

Classical approaches for modelling multiphase flow in porous media use finite differences (FD) for structured meshes and finite volumes for unstructured meshes (e.g. [47], [4], [13]). However, most implementations use the two-point flux approximation (TPFA) to compute the fluxes between cells which is correct only if the mesh is k-orthogonal. This places significant limitations on the geometry of the mesh used to discretize heterogeneous porous media (e.g. [28], [41], [54]). Alternatives have been developed to overcome this problem, such as the multi-point flux approximation (e.g. [1], [45], [46], [56], [61]).

An alternative to FD and FV methods is the use of finite elements (FE) together with control volumes (CV), known as the control volume finite element (CVFE) method. Research into the CVFE method for porous media flow dates back to the 1970s (e.g. [35], [11], [22], [23], [17], [18], [30], [5], [19], [24], [53], [33], [40], [39], [50], [36], [43], [42], [49]). This approach combines the flexibility of finite-element discretizations that are well suited to capture complex geologic

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architectures (e.g. Fig. 1), with the capabilities of control-volume methods to produce stable, locally mass-conservative solutions ([50]). Typically, pressure and velocity, and material properties, such as permeability and porosity, are represented FE-wise, but mass conservative properties such as saturation and concentration are represented CV-wise.

In standard CVFE methods, the CVs span the boundaries between contrasting material properties (Fig. 2(A)). This creates a problem when there are contrasts in permeability or capillary entry pressure across the boundary. A number of studies have considered the case of contrasting capillary entry pressure, where appropriate conditions need to be implemented at the boundary to ensure the correct physical representation (see [15], [16], [31], [32] and [14]). Here, we focus on the geologically common situation in which where there are significant permeability contrasts across the boundary. In this case, the use of CVs that span the boundary causes mass to artificially leaks out of high permeability domains and into low (or zero) permeability domains and vice-versa (e.g. [7], [44], [2], [52], Fig. 1(B)). Fluid saturation and component concentration are therefore smeared across neighbouring elements ([2]). This issue has led some authors to argue that, despite the advantages outlined above, CVFE methods are not suitable for modelling multiphase flow in highly heterogeneous porous media (e.g. [21], Fig. 2(A)).

Several recent papers have addressed the problem of CVs that span domain boundaries in heterogeneous porous media. [44] separated the CVs at FE interfaces that correspond to domain boundaries, and employed the average flux between elements at the interface. However, this approach does not guarantee local mass conservation. [7] used the boundary FE nodes, which reduces the ‘smearing’ because each CV spans at most two FEs (Fig. 2(B)). However, the approach is numerically expensive, as the number of degrees of freedom at FE interfaces can be more than nine times the number of degrees of freedom at FE nodes in a tetrahedral mesh. Furthermore, the smearing effect is not eliminated, as CVs still span more than one FE. Thus, higher mesh resolution is still required at domain boundaries to reduce the ‘smearing’ effect. [52] introduced a new element pair which eliminates the ‘smearing’ effect by employing CVs that are discontinuous between FEs. The method is numerically consistent because pressure is also discontinuous. Their results were promising, but the method was implemented only in 2D. Most models of interest in porous media flow are 3D.

The first key aim of this paper is to develop and implement a new CVFE method in 3D that does not require the use of control volumes (CVs) that span domain boundaries in heterogeneous porous media. We implement discontinuous CVs here by allowing pressure to be discontinuous between elements, using the element pair first presented by [52] which has a discontinuous 1st-order representation for pressure, and a discontinuous 2nd-order representation for velocity. The (discontinuous) pressure and velocity fields are solved using a FE approach and saturation is updated within CVs, but the CVs do
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