First direct detection of an exoplanet by optical interferometry

Astrometry and K-band spectroscopy of HR 8799 e

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ABSTRACT

Aims. To date, infrared interferometry at best achieved contrast ratios of a few times 10−4 on bright targets. GRAVITY, with its dual-field mode, is now capable of high contrast observations, enabling the direct observation of exoplanets. We demonstrate the technique on HR 8799, a young planetary system composed of four known giant exoplanets.

Methods. We used the GRAVITY fringe tracker to lock the fringes on the central star, and integrated off-axis on the HR 8799 e planet situated at 390 mas from the star. Data reduction included post-processing to remove the flux leaking from the central star and to extract the coherent flux of the planet. The inferred K band spectrum of the planet has a spectral resolution of 500. We also derive the astrometric position of the planet relative to the star with a precision on the order of 100 μas.

Results. The GRAVITY astrometric measurement disfavors perfectly coplanar stable orbital solutions. A small adjustment of a few degrees to the orbital inclination of HR 8799 e can resolve the tension, implying that the orbits are close to, but not strictly coplanar. The spectrum, with a signal-to-noise ratio of ≈5 per spectral channel, is compatible with a late-type L brown dwarf. Using Exo-REM synthetic spectra, we derive a band spectrum of the planet has a spectral resolution of 500. We also derive the astrometric position of the planet as close as 390 mas to its parent star.

Key words. stars: individual: HR 8799 – planets and satellites: atmospheres – planet-star interactions – techniques: interferometric

1. Introduction

Obtaining accurate orbits, masses, and atmospheric spectra of directly imaged planets is key to determining their natures and, ultimately, their formation histories. Here we demonstrate the power of a new technique, using optical interferometry, to obtain this information for an exoplanet as close as 390 mas to its parent star.

Because they are better known, the spectra of brown dwarfs (BD) are often used as references to classify the young exoplanet atmospheres. More precisely, the L-T transition is an important observable for understanding the evolution of atmospheres as a function of temperature. At lower temperatures (<1200 K), opacity changes due to the transition of CO to methane in chemical equilibrium, and the likely disappearance of silicate and iron clouds under the photosphere, makes the spectral appearance of T-type BDs bluer. On the contrary, young giant exoplanets of temperature ≈1000 K still have redder near-infrared colors typical of late-L BDs. This is explained by the relatively low surface gravity (g ≤ 104 cm s−2), and hence larger scale heights, in planetary atmospheres. However, the exact cause (cloud properties and/or vertical chemical mixing) is not properly understood (Allard et al. 2012). Once the problem of cloud formation and chemical processes are solved (Helling et al. 2014; Moses et al. 2016), the determination of the molecular composition of exoplanet atmospheres will become a crucial tool toward understanding the formation process of planets: the
Fig. 1. Colored lines are HR 8799 e visibilities $|V_{\text{planet}}|$, as defined by Eq. (1), obtained from the ratio between the coherent flux observed on the planet and on the star. The underlying dotted colored lines correspond to the errors estimated by the pipeline. The theoretical stellar visibility corresponds to the black dashed line (uniform disk of diameter 0.342 mas). The upper horizontal dotted black line corresponds to the observed incoherent flux (stellar flux leaking in the planet’s field). The lower horizontal dotted black line corresponds to the theoretical visibility of a planet 10.7 mag fainter than the star. Right inset: coverage of the spatial frequency plane, east is to the right. The arrow indicates the direction of the planet situated to the northwest of the star.

atomic ratio or even isotope ratio will change depending on the conditions of formation. For example, the C-to-O ratio in the gas of a protoplanetary disk is predicted to increase outwards past the H$_2$O ($\approx$140 K), CO$_2$ ($\approx$50 K), or even CO ($\approx$20 K) ice-lines (Oberg et al. 2011): C/O in the planet atmosphere should therefore change depending on where in a disk planets form and how much gas and how many planetary systems they accrete (Mordasini et al. 2016). Similarly, the D-to-H ratio in planets can be linked to the accretion of icy bodies (Feuchtgruber et al. 2013) and can be seen in molecular absorption spectra (Mollière & Snellen 2019).

The study of cloud properties and composition requires spectral information, which can currently only be obtained by two means: transit spectroscopy or thermal emission spectroscopy. Transit spectroscopy is best for characterizing planets in close orbit around the host star, with puffy (inflated) irradiated atmospheres (Crossfield 2015, and references herein). Thermal emission spectroscopy is more adapted to young, self-luminous planets in orbits with a semimajor axis of a few tens of AU (Crossfield 2015, and references herein). Thermal emission spectroscopy can be seen in molecular absorption spectra (Mollière & Snellen 2019).

Sect. 2 we present the GRAVITY observation of HR 8799 e and the data reduction. HR 8799 is a bright ($K = 5.24$ mag), nearly ($d = 39.4 \pm 0.1$ pc) A5 star. We know that at least four planets are orbiting the star (the first three discovered by Marois et al. 2008). In Sect. 3 we present a new astrometric measurement of the fourth planet ($K = 15.9$ mag), discovered in 2010 by Marois et al. (2010) at 368 ± 9 mas from its host star. The youth of the star ($\approx$30 Myr, member of the Columba Association Malo et al. 2013), implies that the planet is still warm from its initial gravitational energy. In Sect. 4 we use the $K$-band spectra and photometry to constrain its spectral type, temperature, and radius. Finally, in Sect. 5, we summarize our results and briefly address the prospects of the interferometric technique.

2. Observations and data reduction

The observations were obtained with the VLTI using the four 8 m Unit Telescopes and the GRAVITY instrument (Eisenhauer et al. 2011; Gravity Collaboration 2017) on 28 August 2018. GRAVITY can observe two objects located in the VLTI field of view by simultaneously injecting, at each telescope coudé focus, the light of each object into a separate single-mode fiber. The two fibers have an effective field of view equal to $\approx$60 mas, the $K$-band diffraction limit of a single telescope (Pfuhl et al. 2014). Each object is thus interferometrically observed separately, but an ultraprecise laser telemetry constantly monitors the differential optical path between the two objects. The first fiber of GRAVITY was placed on the star for fringe tracking (Lacour et al. 2019) and phase referencing. The second fiber was centered sequentially on the planet and on the star, situated at $\approx$390 mas from each other. This second fiber fed the science spectrometer configured at medium resolution ($R = 500$). Observations of the star were used to calibrate the observation of the planet. Because of the faintness of the planet, a detector integration time (DIT) of 100 s was required. As the star is more than 10 mag brighter than the planet in $K$ band, a DIT of 1 s was sufficient for the
Table 1. Observing log (data taken on 2018-Aug-28).

| Target  | UT Time  | DIT  | NDIT | Seeing  | Airmass | par. angle |
|---------|----------|------|------|---------|---------|------------|
| Planet  | 04:33:59 | 100 s| 10   | 0.8°   | 4.9 ms  | −164.3°    |
| Star    | 04:51:27 | 1 s  | 50   | 0.5°   | 7.1 ms  | −169.6°    |
| Sky     | 04:52:56 | 1 s  | 50   | 0.5°   | 6.7 ms  | −170.0°    |
| Planet  | 04:54:35 | 100 s| 10   | 0.6°   | 6.2 ms  | −170.6°    |
| Planet  | 05:11:55 | 100 s| 10   | 0.6°   | 6.2 ms  | −176.0°    |
| Sky     | 05:29:27 | 100 s| 10   | 0.4°   | 8.5 ms  | −178.5°    |
| Planet  | 05:46:56 | 100 s| 10   | 0.5°   | 6.3 ms  | −172.9°    |
| Planet  | 06:07:13 | 100 s| 10   | 0.6°   | 5.6 ms  | −166.7°    |
| Star    | 06:24:42 | 1 s  | 50   | 0.8°   | 4.2 ms  | −161.5°    |
| Sky     | 06:26:10 | 1 s  | 50   | 0.8°   | 3.9 ms  | −161.1°    |
| Planet  | 06:28:04 | 100 s| 10   | 0.7°   | 4.9 ms  | −160.5°    |
| Planet  | 06:45:25 | 100 s| 10   | 0.7°   | 6.2 ms  | −155.7°    |
| Sky     | 07:04:02 | 100 s| 10   | 1.0°   | 3.6 ms  | −150.9°    |

Notes. $\tau_0$ is the coherence time in the visual (500 nm); par. angle is the parallactic angle.

The frequency plane and the amplitude of the planet’s visibilities are presented in Fig. 1. The colored dotted lines below the visibilities are the errors estimated by the pipeline. The mean S/N per spectral channel is ~5. The detailed data reduction procedure will be presented by Nowak et al. (in prep.).

3. Retrieval of the spectrum of the planet by assuming a diameter for the planet and a synthetic stellar spectrum: $V_{\text{planet}} = \frac{\text{VISDATA}_{\text{planet}}}{\text{VISDATA}_{\star}} \times \frac{2J_1(\pi\theta_{\text{star}}u)}{\pi\theta_{\text{star}}u}$, (1)

where $J_1$ is a Bessel function of the first kind, of order 1; $\theta_{\text{star}}$ is the stellar diameter; and $u$ is the spatial frequency in rad$^{-1}$.

4. Normalization in phase and amplitude of the remaining coherent flux by the coherent flux observed on the star multiplied by the theoretical visibility function of the star. This gives the complex visibility of the planet $V_{\text{planet}} = \frac{\text{VISDATA}_{\text{planet}}}{\text{VISDATA}_{\star}} \times \frac{2J_1(\pi\theta_{\text{star}}u)}{\pi\theta_{\text{star}}u}$, (1)

where $J_1$ is a Bessel function of the first kind, of order 1; $\theta_{\text{star}}$ is the stellar diameter; and $u$ is the spatial frequency in rad$^{-1}$.

5. Retrival of the spectrum of the planet by assuming a diameter for the planet and a synthetic stellar spectrum: $F_{\text{planet}} = \frac{|V_{\text{planet}}|F_{\text{star}}}{2J_1(\pi\theta_{\text{planet}}u)/\pi\theta_{\text{planet}}u}$, (2)

The stellar diameter is assumed to be $\theta_{\text{star}} = 0.342 \pm 0.008$ mas (Baines et al. 2012) and is plotted as the black dashed line in Fig. 1. The planet diameter is assumed to be negligible at the resolution of the interferometer. For the star, we used a BT-NextGen model ($T = 7400$ K; [Fe/H] = −0.5, and log(g) = 4.0) from Hauschild et al. (1999), scaled for a K-band flux of $3.191 \times 10^{-12}$ W m$^{-2}$ μm$^{-1}$.

1 The pipeline in its version 1.1.2 is currently available at https://www.eso.org/sci/software/pipelines/gravity.

Fig. 2. Keplerian orbit fit of HR 8799e. The black point is the GRAVITY measurement, and the gray points are from previous astrometry (Konopacky et al. 2016; Wang et al. 2018a). The yellow lines are 250 random draws from the posterior. The orbit determination is currently limited by the mas-level astrometry of the previous epochs (top inset). Image magnified by ~200x to display the uncertainties in the GRAVITY astrometry. The plotted error bars are rotated to be aligned with the principal axes of the error ellipse. Bottom inset: image magnified by ~2x to display the uncertainties in the previous measurements.

Table 2. Astrometry on HR 8799 e.

| MJD   | δRA  | δDec | Covariance |
|-------|------|------|------------|
| 58358.190 | −357.63 | 163.59 |
| 58358.205 | −357.68 | 163.63 |
| 58358.217 | −357.54 | 163.05 |
| 58358.241 | −357.58 | 163.28 |
| 58358.255 | −357.61 | 163.12 |
| 58358.269 | −357.62 | 163.22 |
| 58358.282 | −357.80 | 163.41 |

Global: $−357.64 \pm 0.07$ 163.34 ± 0.18 $−0.00668$

In the same way as we can disentangle the complex coherent energy from the star and the planet, it is also possible to fit the wavelength dependence of the phase, which is tantamount to measuring a separation. Each fit, for each baseline, gives a χ² minimum for an optimal optical path difference (OPD). This χ² minimum is at the uncertainty is 55 μas. Orthogonal to that baseline (PA = 168°) the uncertainty is 190 μas. The plate scale and true north error is negligible at that level (>50 μas) as the spatial frequencies are defined by the physical position of the telescopes. Atmospheric dispersion is also negligible. A detailed description of the error

science channel observations of the star. Seeing conditions were average to good. The log of the observations is presented in Table 1, where exposures on the planet are shown along the sky and stellar calibration exposures.
terms of interferometric astrometry is presented in Lacour et al. (2014).

As this astrometry is an order of magnitude more precise than the best measurements made by direct imaging instruments (Wang et al. 2018a), we investigate the orbital constraints provided by this datapoint. We fit a single Keplerian orbit by combining this measurement with the astrometry reported in Konopacky et al. (2016) and Wang et al. (2018a). Given the asymmetry in the GRAVITY measurement, we fit for the location of the planet at the GRAVITY epoch in a rotated frame that is aligned with the two principal axes of the error ellipse (top inset of Fig. 2). We use the parallel-tempered Markov chain Monte Carlo sampler (Foreman-Mackey et al. 2013; Vosden et al. 2016) in the orbit fitting code orbitize (Blunt et al. 2019) to estimate the orbital parameters and find a semimajor axis of 16.4^{+2.1}_{-1.1} AU, an eccentricity of 0.15 ± 0.08, and an inclination of 25° ± 8°. A single 100 μas precision point is able to significantly constrain the position of the planet at the epoch of observation, but the determination of the planet’s velocity, acceleration, and orbital properties are still dominated by the mass-level uncertainties in the previous astrometry. We therefore defer a thorough dynamical study to a time when multi-epoch orbital monitoring of the planet with VLTI/GRAVITY has been obtained.

We can also compare the location of the planet measured by GRAVITY with the 2014 version of the model

\[ \text{GRAVITY data} \]

\[ \text{SPHERE photometry} \]

\[ \text{GPI data} \]

\[ \text{Exo-REM T=1150K / log(g)=4.3} \]

\[ \text{Luhman 16A} \]

\[ \text{GPI data} \]

\[ \text{SPHERE photometry} \]

\[ \text{GRAVITY data} \]

\[ \text{Reduced } \chi^2 \text{ as a function of effective temperature and surface gravity from a grid of Exo-REM models (Charnay et al. 2018). The yellow contours correspond to the 5σ error, indicating a valley of possible parameters at } T=1150 \text{K, } \log(g)=4.3 \text{.} \]
in agreement with Bonnefoy et al. (2016) and Greenbaum et al. (2018). A T-type BD spectrum is clearly ruled out. The reduced χ² increases to 3 for spectral types ≈L4, which is significant with 230° of freedom. Similarly, we fitted a grid of BT-Settl 2014 synthetic spectra (Baraffe et al. 2015) to derive a temperature and a surface density. The best fit was obtained for a temperature of 1400 K and a surface gravity of 10^4 cm s^-2. This corresponds to a planetary radius of 0.8 R_Jup.

This radius being incompatible with evolutionary models, we turned to the Exo-REM model (Baudino et al. 2015; Charnay et al. 2018). We found that values of 1150 ± 50 K and log(g) = 4.3 ± 0.3 (error bars 3σ) correctly reflect the spectrum in the K band (Fig. 4). According to the luminosity estimated by the model, it corresponds to a radius of R = 1.17^{+0.13}_{-0.11} R_Jup. This gives a model-dependent estimate of the mass of HR 8799 e of 10^4 M_J. Simulations with Exo-REM predict that the LT transition occurs at a lower effective temperature for exoplanets than for field brown dwarfs, due to effects of pressure on the formation of iron and silicate clouds. This trend is apparent in Fig. 4, where the LT transition corresponds to a sudden increase in χ² and occurs at an effective temperature just 100 K lower than our best fit.

5. Summary and conclusions

Interferometric astrometry, an order of magnitude more accurate than direct imaging, opens new possibilities to study the dynamics of planetary systems. With just a single data point from GRAVITY, we can strongly disfavor perfectly coplanar stable orbits for the HR 8799 planets. As the dynamics probe the masses, formation history, and the future system architecture, interferometric orbital monitoring at the 10–100 µas level can significantly improve our understanding of directly imaged systems.

Based on the K-band spectrum, we confirm a spectral type (≈L7), equivalent to a higher temperature BD. The discrepancy between spectral type (T > 1400 K; Schweitzer et al. 2002) and effective temperature derived from wide-band photometry (T < 1200 K) can be solved by using models taking the lower surface gravity into account. It is interesting to note that the GRAVITY K-band spectrum does constrain this low surface gravity, as shown by the residual map in Fig. 4. We determine a surface gravity compatible with a 10 M_Jup planet.

The interferometric technique brings unique possibilities to characterize exoplanets. With the technique described here, any planet with Kmag ≤ 19, ΔKmag ≤ 11, and separation ≥100 mas is, in theory, observable with GRAVITY. The numbers are still to be refined, but it would mean that GRAVITY could observe most of the known imaged planets, and maybe in the near future planets detected by radial velocity. Furthermore, the good normalization of the continuum spectrum offers new ways to measure the column density of molecules without the need for smoothing and cross-correlation (e.g., Snellen et al. 2014; Konopacky et al. 2013). Finally, the idea that an interferometer can resolve the surface of exoplanets, giving radius and resolving clouds patchiness, is now becoming more plausible. However, it would require an interferometer with baselines on the order of 10 km. This could be a goal for ESO after ELT construction.

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