Materialized View Selection and Maintenance Using Multi-Query Optimization

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Abstract

Because the presence of views enhances query performance, materialized views are increasingly being supported by commercial database/data warehouse systems. Whenever the data warehouse is updated, the materialized views must also be updated. However, whereas the amount of data entering a warehouse, the query loads, and the need to obtain up-to-date responses are all increasing, the time window available for making the warehouse up-to-date is shrinking. These trends necessitate efficient techniques for the maintenance of materialized views.

In this paper, we show how to find an efficient plan for maintenance of a set of views, by exploiting common subexpressions between different view maintenance expressions. These common subexpressions may be materialized temporarily during view maintenance. Our algorithms also choose subexpressions/indices to be materialized permanently (and maintained along with other materialized views), to speed up view maintenance. While there has been much work on view maintenance in the past, our novel contributions lie in exploiting a recently developed framework for multiquery optimization to efficiently find good view maintenance plans as above. In addition to faster view maintenance, our algorithms can also be used to efficiently select materialized views to speed up workloads containing queries.

1 Introduction

Materialization of views can help speed up query and update processing. Views are especially attractive in data warehousing environments because of the query intensive nature of data warehouses. However, when a warehouse is updated, the materialized views must also be updated. Typically, updates are accumulated and then applied to a data warehouse. Loading

\textsuperscript{*}Work partly supported by a Govt. of India, Department of Science and Technology Grant, and by an IBM University Partnership Program Grant. The work of Prasan Roy was supported by an IBM Research Fellowship. Ramamritham was also supported in part by NSF grant IRI-9619588.
of updates and view maintenance in warehouses has traditionally been done at night. While
the need to provide up-to-date responses to an increasing query load is growing and the amount
of data that gets added to data warehouses has been increasing, the time window available for
making the warehouse up-to-date has been shrinking. These trends call for efficient techniques
for maintaining the materialized views as and when the warehouse is updated.

Given multiple views, the view maintenance problem can be seen as computing the expres-
sions corresponding to the “delta” of the views, given the “delta”s of the base relations that are
used to define the views. The contributions of this paper lie in the exploitation of the Multi-
Query Optimization (MQO) framework along with our recently developed efficient algorithms
for MQO, to compute the delta expressions corresponding to the multiple views defined in a
data warehouse.

It is not difficult to motivate that query optimization techniques are important for choosing
an efficient plan for maintaining a view. For example, consider the expression \((A \bowtie B) \bowtie C\),
where \(A\), \(B\) and \(C\) are multisets (i.e., relations with duplicates). Given that the multiset of
tuples \(\delta_C^+\) is inserted into \(C\), the change to the view is given by \((A \bowtie B) \bowtie \delta_C^+\). This expression
can equivalently be computed as \((A \bowtie \delta_C^+) \bowtie B\) and by \((B \bowtie \delta_C^+) \bowtie A\), one of which may be
substantially cheaper to compute. Further, in some cases the view may be best maintained
by recomputing it, rather than by finding the differentials as above. Vista \[Vis98\] describes
how to extend the Volcano query optimizer \[GM91\] to choose the best plan for computing the
differential of the result of an expression.

Given a set of queries, multiquery optimization \[Sel88\] provides the possibility of reducing
costs by computing shared subexpressions once, materializing them temporarily, and reusing
them where required in the given set of queries. Although multiquery optimization was earlier
viewed as expensive, our recent work \[RSSB00\] has provided efficient algorithms for multiquery
optimization, making it practical. In this paper, we provide practical solutions to the problem
of optimizing the update of a set of materialized views, by exploiting these algorithms.

Specifically, our contributions are as follows.

1. We extend the multiquery optimization algorithms to find the best plan for computing
the differential of a set of expressions, by exploiting shared subexpressions.
Sharing of subexpressions occurs when multiple views are being maintained, since related
views may share subexpressions, and as a result the maintenance expressions may also
be shared. Furthermore, sharing can occur even within the plan for maintaining a single
view, as we illustrate later in the paper.

Our algorithms choose shared expressions to be temporarily materialized during view
maintenance, and choose view maintenance plans that utilize these temporarily material-
ized results.

2. Just as the presence of views allows queries to be evaluated more efficiently, the mainte-
nance of these views can be made more efficient by the presence of additional views/indices
That is, given a set of materialized views to be maintained, we need to choose what additional indices and views should be materialized to minimize overall view maintenance costs.

The choice of additional views must be done in conjunction with choosing plans for maintaining the views. For instance, a plan that seems quite inefficient could become the best plan if some intermediate result of the plan is chosen to be materialized and maintained.

Our contribution here is to show how to extend the multiquery optimization algorithms of [RSSB00] to tackle the problems of selecting permanent materialized views, in conjunction with choosing the best plans for updating the views.

We show how to cleanly integrate the choice of expressions/indices to be permanently materialized, with the choice of expressions/indices to be temporarily materialized.

It is worth pointing out that although our focus in this paper is to speed up view maintenance, our algorithms can also be used to choose extra temporary and permanent views in order to speed up a workload containing queries and updates (that trigger view maintenance).

There has been much earlier work on choosing a set of views to be materialized and maintained to optimize given workloads of queries and updates. The major differences between our work and earlier work can be summarized as follows (we outline the differences in detail in Section 2):

1. Given a set of related materialized views, temporarily materializing common subexpressions could have significant benefit. However, earlier work did not consider how to exploit common subexpressions by temporarily materializing them because of their focus on permanent materialization and common subexpressions involving differential relations cannot be permanently materialized.

2. The earlier work does not cover efficient techniques for the implementation of materialized view selection algorithms, in particular, their integration with query optimizers. In the context of materialized view maintenance, this is an important problem since the cost of view maintenance can be reduced by the presence of (additional) indices on relations, and of appropriate extra materialized views.

In contrast, we show how to efficiently choose views/indices to be (permanently) materialized by extending the multiquery optimization algorithms of [RSSB00].

The rest of the paper is organized as follows. We outline related work in Section 2, and provide the reader with some background in view maintenance in Section 3. We describe the DAG structure used to represent queries in Section 4, and algorithms to find optimal update plans (without materializing additional views) in Section 5. Section 6 presents an optimized greedy algorithm for selecting extra views for materialization. Section 7 outlines results of a performance study, and Section 8 concludes the paper.
2 Related Work

There has been a large volume of research on incremental view maintenance in the past decade. Amongst the early work on computing the differential results of operations/expressions was Blakeley et al. [BCL86]. More recent work in this area includes [GL97, CGL+96, MQM97]. Gupta and Mumick [GM95] provide a survey of view maintenance techniques.

Blakeley et al. [BCL86] and Ross et al. [RSS96] noted that the computation of the expression differentials has the potential for benefiting from multiquery optimization. In the past, multiquery optimization was viewed as too expensive for practical use. As a result they did not go beyond stating that multiquery optimization could be useful for view maintenance. Our recent work in [RSSB00] provides efficient heuristic algorithms for multiquery optimization, and demonstrates that multiquery optimization is feasible and effective.

There has been much work on selection of views to be materialized. One notable early work in this area was by Roussopolous [Rou82]. Ross et al. [RSS96] considered the selection of extra materialized views to optimize maintenance of other materialized views/assertions, and mention some heuristics. Labio et al. [LQA97] provide further heuristics. The problem of materialized view selection for data cubes has seen much work, such as [HRU96], who propose a greedy heuristic for the problem. Gupta [Gup97] and Gupta and Mumick [GM99] extend some of these ideas to a wider class of queries. However, (a) none of the above papers consider implementation details that are important for efficient selection of views, and (b) none of these consider how to optimize view maintenance expressions.

Vista [Vis98] describes how to extend the Volcano query optimizer to optimize view maintenance. However, she does not consider the materialization of expressions, whether temporary or permanent. Optimizations that exploit knowledge of foreign key dependencies can be used to detect that certain join results involving differentials will be empty [QGMW96, Vis98].

Roy et al. [RSSB00] consider how to perform multiquery optimization by selecting subexpressions/indices for temporary materialization. They present important optimizations of a greedy heuristic for materialized view selection that makes the heuristic practical. However, they do not consider updates or view maintenance, which is the focus of this paper. We utilize the optimizations proposed in [RSSB00], but the extensions required to to take update costs into account, and optimize view maintenance expressions, are non-trivial.

There has been earlier work on multiquery optimization, including [Sel88, SSN94, SG90] and more recently [SV98], but none of these consider updates.

3 Background and Motivation

We assume that updates (inserts/deletes) to relations are logged in corresponding *delta* relations, which are made available to the view refresh mechanism. We assume for each relation \( r \), there are two relations \( \delta^+_r \) and \( \delta^-_r \) denoting, respectively, the (multiset of) tuples inserted into and deleted from the relation \( r \).

The view refresh mechanism is invoked as part of an update transaction for immediate update, or periodically for deferred updates. In the second case, updates performed by many
transactions may be collected together in the *delta* relations $\delta_r^+$ and $\delta_r^-$ for a relation $r$. Our techniques work regardless of whether the updates are immediate or deferred.

### 3.1 Computing the Differential of an Operation

There is a considerable amount of literature on computing differentials of operations, as outlined in Section 2. For completeness, we briefly review techniques for computing the differential of an operation in the multiset relational algebra.

#### 3.1.1 Differentials of Joins

Consider a multiset join $A \bowtie B$, and suppose $A$ and $B$ are updated by inserting the multisets of tuples $\delta_A^+$ and $\delta_B^+$ respectively. Let $A^{old}$ and $B^{old}$ refer to the old values of $A$ and $B$, that is their contents before the update. The multiset of tuples that get added to the view $V$ are denoted by $\delta_V^+$, and can be computed as:

$$\delta_V^+ = (\delta_A^+ \bowtie B^{old}) \cup (A^{old} \bowtie \delta_B^+) \cup (\delta_A^+ \bowtie \delta_B^+)$$

View $V$ is then updated as follows: $V \leftarrow V \cup \delta_V^+$

Similarly, if tuples $\delta_A^-$ and $\delta_B^-$ are deleted from $A$ and $B$ respectively, the multiset of tuples

$$\delta_V^- = (\delta_A^- \bowtie B^{old}) \cup (A^{old} \bowtie \delta_B^-) \cup (\delta_A^- \bowtie \delta_B^-)$$

get deleted from $V$, which is then updated by: $V \leftarrow V - \delta_V^-$.

Updates can be modeled as deletes followed by inserts. If both inserts and deletes are present on a relation, we get a more complex expression for updating the relation.

$$V \leftarrow V \cup (A^{old} \bowtie \delta_B^+) \cup (\delta_A^+ \bowtie B^{old}) \cup (\delta_A^+ \bowtie \delta_B^-) - (A^{old} \bowtie \delta_B^-) - (\delta_A^+ \bowtie B^{old}) \cup (\delta_A^- \bowtie \delta_B^-)$$

In contrast if only one input, say $A$, is updated by only insertion the change in the view is much easier to compute:

$$\delta_V^+ = \delta_A^+ \bowtie B^{old}$$

and similarly for deletions on $A$,

$$\delta_V^- = \delta_A^- \bowtie B^{old}$$

To keep expressions simple (and for another reason which we describe later in Section 3.2.3) we assume that updates are propagated one relation at a time, and only one type of update at a time. This simply means we compute the effect of all inserts on $A$, then update $A$ with $\delta_A^+$, then compute the effects of all deletes on $A$, update $A$ with $\delta_A^-$, and then proceed with inserts to $B$, and then with deletes from $B$.

The net result is the same as if the more complicated expressions are used, but the expressions we need to deal with are much simpler. Note that an operation may have two complex expressions as inputs, and if both use a particular relation, even with this restriction there may be differential results on both its inputs, in which case the more complex expression allowing differentials on both inputs must be used.
3.1.2 Differentials of Other Operations

If the result of a groupby/aggregate operation, such as $A \sum B (E)$, has been materialized (and the aggregate function is distributive), the change in the aggregate result can be computed using only the changes ($\delta^+_E$ and $\delta^-_E$) to the input $E$, and the old result of the aggregation.\footnote{For some operations like average, the count of tuples in each group must also be materialized. Even for the sum operation, the count of tuples is needed to deal with deletions.}

The group-by/aggregation operation is executed on the tuples from the delta relations, and the results are merged into the existing materialized view using a merge operation. For more details, see, e.g., [GM95], and for extensions to operations such as median, see [RSSS94].

To compute the differential result of an aggregate/grouping operation whose result has not been materialized, we would have to recompute the aggregate values for all groups which are affected by the update. This may involve significant extra work.\footnote{There are techniques, such as [CGL+96, MQM97], that use differentials of more complex forms, such as changes in the value of an aggregate result, to avoid recomputing aggregate values in some special cases. Our techniques can be extended to deal with such differentials, but for simplicity we do not consider such techniques here.}

Standard techniques are available for computing the differentials of other operations, such as duplicate elimination (and projection), and outer joins [GL95, GJM97]. We omit details but note that we can use these techniques without any changes to our optimization algorithms.

3.2 Computing the Differential of an Expression

Views are defined by potentially complex expressions, hence we need to find the differential of an entire expressions.

3.2.1 Generating a Differential Expression

Techniques, such as that of [GL95] can be used to generate an expression that computes the differential of a given expression. However, the resultant expression can be very large – exponential in the size of the query. For instance consider the view $V = A \times B \times C$, with inserts on all three relations. The differential in the result of $V$ can be computed as

$$
(\delta^+_A \times B \times C) \cup (A \times \delta^+_B \times C) \cup (A \times B \times \delta^+_C) \cup (A \times \delta^+_B \times \delta^+_C) \cup (\delta^+_A \times B \times \delta^+_C) \cup (\delta^+_A \times \delta^+_B \times C) \cup (\delta^+_A \times \delta^+_B \times \delta^+_C)
$$

The size of this expression is exponential in the number of relations. Optimizing such large expressions can be quite expensive, since query optimization is exponential in the size of the expression. There are many common subexpressions in the above expression, and the above expression could be simplified by factoring, to get:

$$
(\delta^+_A \times B \times C) \cup ((A \cup \delta^+_A) \times \delta^+_B \times C) \cup ((A \cup \delta^+_A) \times (B \cup \delta^+_B) \times \delta^+_C)
$$

But creating simplified forms of differential expressions is difficult with more complex expressions containing operations other than join.

Therefore our algorithms use an alternative technique, which we outline in the next section.
3.2.2 Propagating Updates Up An Expression

An alternative to generating a differential expression is to propagate differentials up an expression \[\text{Rou82, RSS96}\]. Propagation is best understood by visualizing an expression as a tree. The differential of a node in the tree is computed using the differential (and if necessary, the old value) of its inputs, as described earlier. We start at the leaves of the tree, and proceed upwards, computing the differential expressions at each node.

For example, consider an expression \((A \bowtie B) \bowtie C\), and suppose we wish to propagate inserts to \(A\). We can do so by first computing the differential of the node \(A \bowtie B\) as \(\delta^+ A \bowtie B\). We then join this differential with \(C\), which is the other input of its parent node, to get the differential of the parent.

As mentioned earlier, if there are updates to multiple relations, we propagate one type of update to one relation at a time. Doing so simplifies the expressions for computing the differentials, as outlined in Section 3.1, and permits a different evaluation plan to be chosen for each expression; this is essential for efficient view maintenance, as we will see next, in Section 3.2.3.

The process of computing the differential of an expression can be expressed purely in terms of how to compute the differentials for each operation in the expression. There is no need to rewrite the entire expression. Note also that the procedure for computing differentials of an expression can be easily extended to handle expressions using new types of operations, so long as we have a way of incrementally computing the differential of the operation.

3.2.3 The Role of Query Optimization

Consider an expression \(A \bowtie (B \bowtie C)\), and suppose tuples are inserted into \(A\). We can compute the differential of the result as \(\delta^+ A \bowtie (B \bowtie C)\). If we compute this expression as shown, we would need to compute \(B \bowtie C\), which does not involve any \(\delta\) relation, and hence may be large and expensive. A better way of evaluating the differential may be \((\delta^+ A \bowtie B) \bowtie C\). Note that the two variants are logically equivalent.

Thus, for efficient differential computation, query optimization must be applied to the update expressions to choose the cheapest variant, as proposed in \[\text{Vis98}\].

Furthermore, note that if we wish to compute the differential when tuples are inserted into \(C\), the plan \((\delta^+ C \bowtie B) \bowtie A\) or \((\delta^+ C \bowtie A) \bowtie B\) may be preferable to \((A \bowtie B) \bowtie \delta^+ C\). Thus, using a single expression, such as \((A \bowtie B) \bowtie C\) to propagate differentials to \(A\), \(B\) and \(C\) is likely to perform badly for at least one of the differentials.

For this reason, we propagate differentials of only one relation at a time, and choose a separate plan for each differential propagation.

We use a query optimizer for choosing best plans for such propagation, and our optimizer uses a DAG representation that compactly represents all expressions equivalent to a given expression. Since all alternative expressions above are available, the best one can be chosen for the propagation of each differential. We present details in Sections 4 and 5.
3.3 The Role of Multi-Query Optimization in View Update

Multi-query optimization attempts at exploiting common sub-expressions within a query, or across queries in a batch of queries submitted together, to reduce the query evaluation cost. In the context of view update, sharing can occur across the tasks of computing differentials of different views, or even within the task of computing the differential of a single view, as we show below.

It is easy to see that related queries may share subexpressions, and if so, it may be best to compute the shared subexpression once, materialize it, and reuse it. However, this decision must be done in a cost based manner, as the following example from [RSSB00] illustrates.

Example 3.1 Let $Q_1$ and $Q_2$ be two queries whose locally optimal plans (i.e., individual best plans) are $(R \bowtie S) \bowtie P$ and $(R \bowtie T) \bowtie S$ respectively. The best plans for $Q_1$ and $Q_2$ do not have any common sub-expressions. However, if we choose the alternative plan $(R \bowtie S) \bowtie T$ (which may not be locally optimal) for $Q_2$, then, it is clear that $R \bowtie S$ is a common sub-expression and can be computed once and used in both queries. This alternative with sharing of $R \bowtie S$ may be the globally optimal choice.

On the other hand, blindly using a common sub-expression may not always lead to a globally optimal strategy. For example, there may be cases where the cost of joining the expression $R \bowtie S$ with $T$ is very large compared to the cost of the plan $(R \bowtie T) \bowtie S$; in such cases it may make no sense to reuse $R \bowtie S$ even if it were available. $\square$

In the context of view maintenance, if two materialized views have common subexpressions, as in the example above, the expressions for computing the differential of the common subexpression would also be shared.

To illustrate subexpression sharing possibilities within a single view maintenance query, consider a view $V$ defined as in the example below.

Example 3.2 Let view $V = A \bowtie B \bowtie C \bowtie D$. Suppose there are inserts on all four relations.

The differential of $V$ can then be computed using

$$(\delta^+_{A} \bowtie B \bowtie C \bowtie D) \cup ((A \cup \delta^+_{A}) \bowtie \delta^+_{B} \bowtie C \bowtie D) \cup ((A \cup \delta^+_{A}) \bowtie (B \cup \delta^+_{B}) \bowtie \delta^+_{C} \bowtie D) \cup ((A \cup \delta^+_{A}) \bowtie (B \cup \delta^+_{B}) \bowtie (C \cup \delta^+_{C}) \bowtie \delta^+_{D})$$

The above expression represents algebraically the effect of propagating differentials one at a time, as described in Section 3.2.2.

Note that there are several potential common subexpressions in the above expression. For instance, if the plans chosen for the first two terms of the above union are $(\delta^+_{A} \bowtie (B \bowtie (C \bowtie D)))$ and $(A \cup \delta^+_{A}) \bowtie (\delta^+_{B} \bowtie (C \bowtie D)))$, then $C \bowtie D$ is a common subexpression of the two. If
the above plans are chosen, the subexpression can be computed once and shared. Similarly, 
\((A \cup \delta_A^+) \bowtie (B \cup \delta_B^+)\) is potentially a common subexpression.

The alternative plans of \(((\delta_A^+ \bowtie B) \bowtie C) \bowtie D)\) and \(((A \cup \delta_A^+) \bowtie \delta_B^+ \bowtie C) \bowtie D)\) offer no sharing possibilities, but may still be cheaper. □

Which the above plans should be used, and whether the common subexpressions should materialized and shared is a decision for the multiquery optimizer to make in a cost-based manner. Thus, it is the job of the multiquery optimizer to find the best overall plan taking sharing possibilities into account.

4 DAG Representation of Queries

Our algorithms use an extended form of the DAG representation of queries used, for instance, in Volcano \[GM91\]. In this section we summarize the DAG representation and terminology from \[RSSB00\].

An AND–OR DAG is a directed acyclic graph whose nodes can be divided into AND-nodes and OR-nodes; the AND-nodes have only OR-nodes as children and OR-nodes have only AND-nodes as children.

An AND-node in the AND-OR DAG corresponds to an algebraic operation, such as the join operation (\(\bowtie\)) or a select operation (\(\sigma\)). It represents the expression defined by the operation and its inputs. Hereafter, we refer to the AND-nodes as operation nodes. An OR-node in the AND-OR DAG represents a set of logical expressions that generate the same result set; the set of such expressions is defined by the children AND nodes of the OR node, and their inputs. We shall refer to the OR-nodes as equivalence nodes henceforth.

4.1 Representing a Single Query

A given query is initially represented directly in the AND-OR DAG formulation. For example, the query tree of Figure \[1\](a) is initially represented in the AND-OR DAG formulation, as
shown in Figure 1(b). Equivalence nodes (OR-nodes) are shown as boxes, while operation nodes (AND-nodes) are shown as circles.

The initial AND-OR DAG is then expanded by applying all possible transformations on every node of the initial query DAG representing the given set of queries. Suppose the only transformations possible are join associativity and commutativity. Then the plans $A \bowtie (B \bowtie C)$ and $(A \bowtie C) \bowtie B$, as well as several plans equivalent to these modulo commutativity can be obtained by transformations on the initial AND-OR-DAG of Figure 1(b). These are represented in the DAG shown in Figure 1(c). We shall refer to the DAG after all transformations have been applied as the *expanded DAG*. Note that the expanded DAG has exactly one equivalence node for every subset of $\{A, B, C\}$; the node represents all ways of computing the joins of the relations in that subset.

4.2 Representing Sets of Queries in a DAG

Queries are inserted into the DAG structure one at a time. When a query is inserted, equivalence nodes and operation nodes are created for each of the operations in its initial query tree. Some of the subexpressions of the initial query tree may be equivalent to expressions already in the DAG. Further, subexpressions of a query may be equivalent to each other, even if syntactically different. For example, query may contain a subexpression that is logically equivalent to, but syntactically different from another subexpression of the query (e.g., $(A \bowtie B) \bowtie C$, and $A \bowtie (B \bowtie C)$).

Before the second subexpression is expanded, the DAG would contain two different equivalence nodes representing the two subexpressions. RSSB00 modifies the Volcano DAG generation algorithm such that whenever it finds nodes to be equivalent (in the above example, after applying join associativity) it *unifies* the nodes, replacing them by a single equivalence node. The Volcano optimizer GM91 already has a hashing-based scheme to efficiently detect repeated expressions, thereby avoiding creation of new nodes that are equivalent to existing nodes. The extension of RSSB00 additionally unifies existing logically equivalent nodes. Another extension is to detect and handle *subsumption* derivations. For example, $\sigma_{A < 5}(E)$ can be computed from $\sigma_{A < 10}(E)$ if they both appear in a set of queries. Similarly, if we have aggregations $dno \mathcal{G}_{\text{sum(Sal)}}(E)$ and $age \mathcal{G}_{\text{sum(Sal)}}(E)$, we can introduce a new equivalence node $dno,age \mathcal{G}_{\text{sum(Sal)}}(E)$ and add derivations of the other two from this one. For more details of unification and subsumption derivations involving selections and aggregation, see RSSB00.

4.3 Physical Properties

It is straightforward to refine the above AND-OR DAG representation to represent physical properties GM91, such as sort order, that do not form part of the logical data model, and obtain a physical AND-OR DAG. The presence of an index on a result is also modeled as a physical property of the result by RSSB00, making the code that handles physical properties

\footnote{For example, an equivalence node is refined to multiple physical equivalence nodes, one per required physical property, in the physical AND-OR DAG.}
also perform index selection. Physical properties of intermediate results are important; for example, if an intermediate result is sorted on a join attribute, the join cost can potentially be reduced by using a merge join. This also holds true of intermediate results that are materialized and shared. Our implementation indeed handles physical properties, including sort orders and indices, but to keep the description simple we do not explicitly consider physical properties.

5 Finding Optimal Plans

We first outline how to find optimal plans for queries, following [RSSB00], and then outline extensions to find optimal plans for view maintenance. In both cases, we assume that the set of views chosen for materialization is fixed. In Section 6 we outline how to integrate the choice of views to materialize with the choice of optimal plans for view maintenance.

5.1 Finding Optimal Plans for Queries

The Volcano optimization algorithm finds the best plan for each node of the expanded DAG by performing a depth first traversal of the DAG. Costs are defined for operation and equivalence nodes. The computation cost of an operation node is

\[ \text{compcost}(o) = \text{cost of executing } (o) + \sum_{e \in \text{children}(o)} \text{compcost}(e) \]

The children of \( o \) (if any) are equivalence nodes. The computation cost of an equivalence node \( e \) is given as

\[ \text{compcost}(e) = \min\{ \text{compcost}(o_i) | o_i \in \text{children}(e) \} \]

and is 0 if the node has no children (i.e., it represents a relation).\(^4\) Note that the cost of executing an operation \( o \) also takes into account the cost of reading the inputs, if they are not pipelined.

Volcano also caches the best plan it finds for each equivalence node, in case the node is re-visited during the depth first search of the DAG.

A simple extension of the Volcano algorithm to find best plans given a set of materialized views is described in [RSSB00]. We outline this extension below.

Let \( \text{reusecost}(m) \) denote the cost of reusing the materialized result of \( m \), and let \( M \) denote the set of materialized nodes.

To find the cost of a node given a set of nodes \( M \) have been materialized, we simply use the Volcano cost formulae above for the query, with the following change. When computing the cost of an operation node \( o \), if an input equivalence node \( e \) is materialized (i.e., in \( M \)), the minimum of \( \text{reusecost}(e) \) and \( \text{compcost}(e) \) is used for computing \( \text{compcost}(o) \). Thus, we use the following expression instead:

\[ \text{compcost}(o, M) = \text{cost of executing } (o) + \sum_{e \in \text{children}(o)} C(e_i, M) \]

where

- \( C(e_i, M) = \text{compcost}(e_i) \) if \( e_i \notin M \)
- \[ = \min(\text{compcost}(e_i, M), \text{reusecost}(e_i)) \] if \( e_i \in M \).

\(^4\)Relation scans are explicitly represented as an operation and assigned a cost.
and compcost for equivalence nodes is defined as before. Thus, the extended optimizer computes best plans for the query in the presence of materialized results. The extra optimization overhead is quite small.

5.2 Extending the DAG Structure for Computing Differentials

We now outline how to extend the DAG structure to represent the differentials of a set of expressions. We first construct the expanded DAG for the given expression (or set of expressions). As in Volcano, each equivalence node in the DAG has a set of logical properties such as the schema of the expression result, and estimated statistics about the result such as number of tuples. Once the best plan is computed for a node, it is cached in case it is needed later during optimization.

If there are \( n \) relations, \( R_1, \ldots, R_n \), we need to store information about the differentials of the node with respect to \( \delta^+_1, \delta^-_1, \delta^+_2, \delta^-_2, \) and so on until \( \delta^+_n, \delta^-_n \). We number these updates as \( 1, \ldots, 2n \), and use these numbers to identify the update.

To optimize differential plans, each equivalence node stores information for the differentials of the expression with respect to each update type, in addition to information about the full result. Each equivalence node \( e \) therefore stores an array of \( 2n \) records, as below. Each odd numbered entry \( 2i - 1, i = 1..n \), of this array contains:

1. logical properties (such as schema and estimated statistics) of the differential of \( e \) with respect to inserts on \( R_i \)
2. the best plan for computing the differential of \( e \) with respect to inserts on \( R_i \)
3. the logical properties of the full result of the equivalence node after inserts and deletes to relations \( R_1, \ldots, R_{i-1} \) have been propagated

Similarly, each even numbered entry \( 2i, i = 1..n \), of this array contains similar information on differentials and best plans with respect to the deletes on \( R_i \), and the logical properties for the full result of the equivalence node after inserts and deletes to relations \( R_1, \ldots, R_{i-1} \), and inserts to \( R_i \) have been propagated.

In addition, as in the original representation, each node stores the best plan for (and cost of) recomputing the entire result of the node after all updates have been made on the base relations.

The logical properties of the differentials are computed by a bottom-up traversal of the DAG. We describe later how the best plans for computing differentials are computed and stored. If an equivalence node does not depend on relation \( R_i \), we flag this during the above bottom-up traversal, and set the plans in entry \( 2i \) and \( 2i + 1 \) to be null.

The traversal also computes and stores an estimate of the execution cost of the differential version of each operation in the DAG (such as a join or an aggregation). The properties of the differentials of its inputs, as well as the full version of the input, where required, are used to compute this estimate.
5.3 Finding Optimal Plans for Updates

We now outline how to find optimal plans for updates, using the above mentioned DAG representation. Recall the example from Section 3.2.3, with the expression being \( A \Join (B \Join C) \), and an insert on \( A \), the plan \( (\delta_A^+ \Join B) \Join C \), is likely to be more efficient than \( \delta_A^+ \Join (B \Join C) \), and should be considered. Luckily for us, the DAG representation of the query represents \((A \Join B) \Join C\) in addition to \( A \Join (B \Join C) \) (see Figure 1).

We now extend the technique for finding optimal plans for queries described in Section 5.1, to find the optimal way of propagating the differential \( \delta_A^+ \).

Some equivalence nodes do not depend on some relations, and their differential with respect to the relation will be empty. Let \( \text{diffChildren}(o, i) \) denote all equivalence node children of \( o \) whose differential is non-empty on update \( i \), and \( \text{fullChildren}(o, i) \) denotes all children of \( o \) whose full results are required to compute the differential of \( o \), in conjunction with \( \text{diffChildren}(o, i) \).

For instance, \( \text{diffChildren} \) for an operation that joins \( A \) with \((B \Join C)\), with respect to an insert on \( B \), is the node \( B \Join C \), and correspondingly \( \text{fullChildren} \) of the node is \( A \).

Given an operation node \( o \) in the DAG, let \( \delta(o, i) \) denote the differential of operation \( o \) with respect to update \( i \). Also let \( \text{localDiffCost}(o, i) \) denote the cost of executing the operations in \( \delta(o, i) \), without counting the cost of generating its inputs.

Similarly, for an equivalence node \( e \), let \( \delta(e, i) \) denote the differential result of \( e \) with respect to update \( i \). Then, the total cost of generating the differential result of an operation node \( o \) with respect to update \( i \), \( \text{diffCost}(o, i) \) can be computed by:

\[
\text{localDiffCost}(o, i) + \sum_{e_j \in \text{diffChildren}(o, i)} \text{diffCost}(e_j, i) + \sum_{e_j \in \text{fullChildren}(o, i)} \text{compcost}(e_j)
\]

The cost of computing the differential of an equivalence node \( e \) with respect to update \( i \) is given as

\[
\text{diffCost}(e, i) = \min \{ \text{diffCost}(o_j, i) | o_j \in \text{children}(e) \}
\]

and is 0 if the node has no children (i.e., it represents a relation or a relation differential). The definition of \( \text{compcost} \) is as defined earlier in Section 5.1, and represents the cost of recomputation of the node after updates have been performed on the database relations.

The above formula is extended for the case where some nodes are materialized, as follows. Note that the full result of a node may be materialized, and independently, any of its differential results may also be (temporarily) materialized. Let the set of materialized results be \( M \); For an operation node \( o \), we compute \( \text{diffCost}(o, M, i) \) as:

\[
\text{localDiffCost}(o, i) + \sum_{e_j \in \text{diffChildren}(o, i)} C(e_j, M, i) + \sum_{e_j \in \text{fullChildren}(o, i)} C(e_j, M)
\]

where \( C \) is defined as follows: if \( \delta(e, i) \) is not materialized (i.e., not in \( M \)),

\[
C(e, M, i) = \min \{ \text{diffCost}(o_j, M, i) | o_j \in \text{children}(e) \}
\]

and if \( \delta(e, i) \) is materialized (i.e., in \( M \)),

\[
C(e, M, i) = \min(\text{reuscost}(e, i), \min \{ \text{diffCost}(o_j, M, i) | o_j \in \text{children}(e) \})
\]

and \( \text{reuscost}(e, i) \) denotes the cost of reusing the materialized result of \( \delta(e, i) \). Also, \( C(e_j, M) \) plays the same role for the full result of node \( e_j \), as defined in Section 5.1.
For an equivalence node \( e \), \( \text{diffCost}(e, M, i) = \min \{ \text{diffCost}(o_j, M, i) | o_j \in \text{children}(e) \} \)
and is 0 if the node has no children (i.e., it represents a relation or a relation differential). That is, \( \text{diffCost} \) represents the cost of computing the differential, even if the differential is materialized.

For each equivalence node \( e \), the operation node corresponding to the minimum cost in the above formula defines the (top node of the) best plan for \( \delta(e, i) \), given that results in \( M \) are materialized.

Further, we can compute the total cost of computing the differential of a node as \( \text{totalDiffCost}(e, M) = \sum_{i=1}^{2n} \text{diffCost}(e, M) \).

We perform a single traversal of the DAG to compute the costs for each equivalence/operation node, based on the above equations. During the traversal we also cache the best (minimum cost) plan computed for each differential, just as we cache the best plans for each full result.

Note that if both inputs to a join \( E_1 \bowtie E_2 \) are expressions using a common relation \( R \), an update to \( R \) results in changes to both inputs, and as a result, the update expression for the join is \( (\delta^+_{E_1} \bowtie E_2) \cup ((E_1 \cup \delta^+_{E_1}) \bowtie \delta^+_{E_2}) \). In this case, a join in the original expression has been converted into a union of two joins. The best plan for each join is found, giving the best plan for the entire expression, and this combined best plan must be stored (and used to compute the cost of finding the differential).

Optimizations that exploit knowledge of foreign key dependencies can be used to detect that certain join results involving differentials will be empty [QGMW96, Vis98]. For instance, if \( r.B \) is a foreign key into \( s.A \), then the join of \( \delta^+_{r} \) and \( r \) will be empty. Based on this, parts of the differential expression can be detected to be empty, and eliminated during optimization.

6 The Greedy Algorithm for Selecting Materialized Views

Till now we assumed that the set of materialized nodes is fixed. We now describe how to integrate the choice of extra materialized views/indices with the choice of best plans for view maintenance. Our algorithm is based on a greedy heuristic. We first present the basic algorithm, then some optimizations, and extensions, below.

6.1 The Basic Greedy Algorithm

As outlined earlier, we first take the given set of materialized views \( V \), and build a DAG structure on the expressions defining the views. The nodes of the DAG corresponding to views in \( V \) are marked as already chosen for materialization.

We consider both full and differential results for materialization. A result is identified by a node and an update number (in our implementation a full result is identified by the update number 0, and differential results by numbers 1...2n).

If a result is chosen for temporary materialization, we must take into account the cost of computing it. And if it is chosen for permanent materialization, we must take into account the cost of maintaining it (we need not consider the cost of initial materialization since it is a one time cost).
Procedure Greedy

Input: Expanded DAG for $\mathcal{V}$, the initial set of materialized views, and the set of candidate equivalence nodes (and their differentials) for materialization

Output: Set of nodes/differentials to materialized

$X = \mathcal{V}$

$Y =$ set of candidates equivalence nodes/differentials for materialization

while ($Y \neq \phi$)

Pick the node $x$ with the highest $benefit(x, X)$

if ($benefit(x, X) < 0$)

break; /* No further benefits to be had, stop */

$Y = Y - x$; $X = X \cup \{x\}$

return $X$

Figure 2: The Greedy Algorithm

The cost of maintaining a node incrementally is the sum of the costs of its differentials:

$$maintcost(n, M) = totalDiffCost(n, M) + mergeCost(n)$$

where $mergeCost(n)$ denotes the cost of updating the materialized result of $n$ using the differentials.

For a full result $n$, we define

$$cost(n, M) = \min(compcost(n, M) + matcost(n), maintcost(n, M))$$

where $matcost(n)$ denotes the cost of writing out the computed result of $n$. That is, when finding the cost of the full result of a materialized node, we take the minimum of the cost via recomputation and the cost via computing the differentials.

For a differential result $x = \delta(n, i)$, we define

$$cost(x, M) = diffCost(n, M, i) + matcost(x).$$

Given a set $S$ of results (full/differential), let $cost(S, M)$ be defined as

$$cost(S, M) = \Sigma_{q \in S} cost(q, M)$$

Given a set of results $M$ already chosen to be materialized, and a result $x$, the benefit of additionally materializing $x$, $benefit(x, M)$, is defined as:

$$benefit(x, M) = cost(M, M) - (cost(M, \{x\} \cup M) + cost(x, M))$$

Note that $(cost(M, \{x\} \cup M) + cost(x, M))$ is equivalent to $cost(M \cup \{x\}, M \cup \{x\})$.

Figure 2 outlines a greedy algorithm that iteratively picks nodes to be materialized. The procedure takes as input the set of candidate results (equivalence nodes, and their differentials) for materialization. At each iteration, the node $x$ that gives the maximum reduction in the cost if it is materialized, is chosen to be added to $X$.

The procedure not only selects results for maintenance, but also decides on how they should be maintained. Specifically, for full results, it chooses the cheaper of recomputation (including the cost of storing the result), and differential computation (including the cost of performing the computed differential updates). If recomputation is cheaper for a result, and the result was not part of the given set of materialized view, the result can be materialized temporarily during
view maintenance, and discarded later. Differential results that are chosen to be materialized are materialized only temporarily since they are only used during view maintenance.

6.2 Optimizations

The greedy algorithm as described above can be expensive due to the large number of times the function `benefit` is called, (which in turn calls the expensive function `cost()`).

Some important optimizations to the greedy algorithm for multi-query optimization are presented in [RSSB00]. We use two of the optimizations, with some extensions for handling differentials:

1. There are many calls to `benefit` (and thereby to `cost()`) at line L1 of Figure 2, with different parameters. A simple option is to process each call to `cost` independent of other calls. However, observe that the set of materialized nodes which is the second argument of `cost` changes minimally in successive calls — successive calls take parameters of the form `cost(R, \{x\} \cup X)`, where only `x` varies. That is, instead of considering `x_1 \cup X` for materialization, we are now considering storing `x_2 \cup X` for materialization. The best plans computed earlier does not change for nodes that are not ancestors of either `x_1` or `x_2`. It makes sense for a call to leverage the work done by a previous call by recomputing best plans only for ancestors of `x_1` and `x_2`.

   A novel incremental cost update algorithm is presented in [RSSB00]. This algorithm maintains the state of the DAG (which includes previously computed best plans for the equivalence nodes) across calls to `cost`, and may even avoid visiting many of the ancestors of `x_1` (which is unmaterialized) and `x_2` (which is materialized).

   In our context of finding update plans, we have to modify the incremental cost update algorithm slightly.

   (a) If the full result of a node is materialized, we update not only the cost of computing the full result of each ancestor node, but also the costs for the `2n` differentials of each ancestor node since the full result may be used in any of the `2n` differentials. Propagation up from an ancestor node can be stopped if there is no change in cost to computing the full result or any of the differentials.

   (b) If the differential of a node with respect to update `i` is materialized, we update only the differentials of its ancestors with respect to update `i`. Propagation can stop on ancestors whose differentials with respect to `i` do not change in cost.

2. The monotonicity optimization works as follows. With the greedy algorithm as presented above, in each iteration the benefit of every candidate node that is not yet materialized is recomputed since it may have changed.

   The monotonicity optimization is based on the assumption that the benefit of a node cannot increase as other nodes are chosen to be materialized – while this is not always true,
it is often true in practice. The monotonicity optimization makes the above assumption, and does not recompute the benefit of a node $x$ if the new benefit of some node $y$ is higher than the previously computed benefit of $x$. It is clearly preferable to materialize $y$ at this stage, rather than $x$ — assuming monotonicity holds, the benefit of $x$ could not have increased since it was last computed, and it cannot be the node with highest benefit now, hence its benefit need not be recomputed now.

Thus, recomputations of benefit are greatly reduced.

[RSSB00] presents a third optimization based on potential sharability of nodes between queries. This optimization is not relevant here, since even a node that is not sharable may be worth materializing permanently.

For the purpose of this paper, the details of the above optimizations are not critical, but the interested reader may refer to [RSSB00] for details.

The Greedy procedure can be extended in a straightforward manner to consider a workload of queries, along with periodic updates, and to choose the best set of results (and indices) to materialize, to minimize the cost of the queries and view update. Some optimizations are needed to handle large workloads [RSSB00]. We can also introduce limits on space for storing permanently materialized results and temporarily materialized results. Results can then be materialized in the order of benefit per unit space, instead of just benefit.

7 Performance Study

We implemented the algorithm described earlier for finding optimal plans for view maintenance. Like the existing multiquery optimization code, the new code implements index selection along with selection of results to materialize. Our current implementation has a restriction in that it only considers full results for materialization, although a version which also considers differential results for materialization should be ready shortly. Thus our estimated benefits are actually conservative, and we may be able to get even better results once the full implementation is ready. However, the benefits are already very significant.

7.1 Performance Model

We used a benchmark consisting of TPC-D queries (and some variants based on the same TPC-D schema). The performance measure is estimated execution cost, called plan cost in the performance graphs. Our cost model extends the cost model used in the multiquery optimizer, by taking differential computation into account. The cost model used takes into account number of seeks, amount of data read, amount of data written, and CPU time for in-memory processing. Since we do not currently have a query execution engine which we can extend to perform differential view maintenance, we are unable get actual numbers. However, the cost model is fairly sophisticated, and further, benefits for multiquery optimization predicted by the basic cost model have been verified by running rewritten queries on commercial database systems ([RSSB00], and results in a companion paper on query result caching), giving support to the accuracy of estimated benefits.
We provide performance numbers for different percentages of updates to the database relations; we assume that all relations are updated by the same percentage. To model a growing database, we have twice as many inserts as deletes. In our notation, a 10 percent update to a relation consists of inserting 10% as many tuples are currently in the relation, and deleting 5% of the current tuples.

We compare the performance of our greedy algorithm (referred to as Greedy in our discussion and figures) with plain Volcano query optimization extended to choose between recomputation and incremental maintenance of views (referred to as NoGreedy). (The algorithm of [Vis98] falls in the same class as NoGreedy, although the optimization method is somewhat different.) For each query, we present results at different update percentages, ranging from 1% to 80%.

The cost of view maintenance is affected by the presence of indices. Normally, databases have indices on the primary key attributes of each relation, to check for uniqueness. Hence we assume that for each of the TPC-D relations, an index is present on the primary key attributes. However, we also ran our benchmark assuming that no indices are initially present, and found that all required indices got chosen for permanent materialization by our algorithm. Thus, the cost of the plans we generate were not significantly affected by the presence of indices, although the cost of plans without our optimizations rose if indices were not already present.

We assume a TPC-D database at scale factor of 0.1, that is the relations occupy a total of 100 MB. The buffer size is set at 8000 blocks, each of size 4KB, although we also ran some tests at a much smaller buffer size of 1000 blocks. The tests were run on an Ultrasparc 10, with 256 MB of memory.
7.2 Performance Results

Maintaining Individual Views. Figure 3 shows our results on two queries, the first consisting of the join of 4 relations, without aggregation, and the second consisting of aggregation on the same join. As can be seen from the figures significant benefits are to be had, especially at low update percentages, but there are benefits even at relatively high update percentages.

Maintaining a Set of Views. Figure 4 shows our results on two sets of queries, the first containing five queries without aggregation and the second containing five queries with aggregation. The benefit ratio due to Greedy is again excellent at lower update percentages. There is a jump in cost at one point, which is because of the use of an algorithm that depends on an input fitting in memory, and when the input does not fit in memory its cost increases sharply.

Figure 5 shows the results on a set of 10 queries, with indices already present on all primary key attributes, and without any indices present initially; all required indices got chosen for materialization.

Cost of Optimization. For a set of 10 materialized views, each a join of 3 to 4 TPC-D relations, (whose results are shown in Figure 5), the time for Greedy optimization was 31 seconds. Note however that 31 seconds is low compared to the savings of up to 1000 seconds obtained for one run of view maintenance, and besides it is a one-time cost whereas view maintenance is typically at least a daily task in a data warehouse. Thus, the extra cost for our algorithms is worthwhile.

The number of candidates for materialization grows exponentially with the number of relations in a query. We are currently working on techniques to prune the set of candidates, in order to keep optimization time in tight control even with a higher number of relations.

Temporary vs. Permanent Materialization. Out of a total of 1600 results that were
materialized (totalling across many different queries and query sets that we considered, and
across update percentages ranging from 1 percent to 90 percent), we found that for about 1000
the recomputation cost was less, meaning they are materialized temporarily, and for 600 the
maintenance cost was less, meaning they were materialized permanently. At 1 to 5 % update
rates, the ratio was 281 to 306, while at 50 to 90 % update rates, the ratio changed to 360 to
88, in favor of recomputation.

Effect of Buffer Size. With a buffer size of 1000 blocks (instead of 8000 blocks), we found
that the costs of plans with and without Greedy optimization went up, but the increase was
more for recomputation plans and the benefit ratio for small update percentages was actually
more strongly in favor of our algorithms.

8 Conclusions and Future Work

The problem of finding the best way to maintain a given set of materialized views is an important
practical problem, especially in data warehouses/data marts, where the maintenance windows
are shrinking. We have presented solutions that exploit commonality between different tasks in
view maintenance, to minimize the cost of maintenance. Our techniques are easy to implement
on an existing multiquery optimizer. As shown by the results in section 7, our techniques can
generate significant speedup in view maintenance cost, and the increase in cost of optimization
is acceptable. We therefore believe that our results are a timely solution to an important
practical problem.

Future work includes further heuristics to decrease optimization cost, and implementing
extensions to efficiently handle workloads containing queries. We also plan to port the system
to a dynamic query result caching environment; in a companion paper, we study the issue of
selecting results to cache dynamically, in the absence of updates.

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