A comparative study of the mechanical and thermal properties of defective ZrC, TiC and SiC

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ZrC and TiC have been proposed to be alternatives to SiC as fuel-cladding and structural materials in nuclear reactors due to their strong radiation tolerance and high thermal conductivity at high temperatures. To unravel how the presence of defects affects the thermo-physical properties under irradiation, first-principles calculations based on density function theory were carried out to investigate the mechanical and thermal properties of defective ZrC, TiC and SiC. As compared with the defective SiC, the ZrC and TiC always exhibit larger bulk modulus, smaller changes in the Young’s and shear moduli, as well as better ductility. The total thermal conductivity of ZrC and TiC are much larger than that of SiC, implying that under radiation environment the ZrC and TiC will exhibit superior heat conduction ability than the SiC. One disadvantage for ZrC and TiC is that their Debye temperatures are generally lower than that of SiC. These results suggest that further improving the Debye temperature of ZrC and TiC will be more beneficial for their applications as fuel-cladding and structural materials in nuclear reactors.

Cubic silicon carbide (3C-SiC), titanium carbide (TiC) and zirconium carbide (ZrC) are taken as attractive candidates for a variety of applications, including the structural component in fusion reactors, the fuel cladding material for gas-cooled fission reactors and the pressure vessels in Tristructural-isotropic fuel 1–4, due to their excellent physical and chemical properties such as high thermal conductivity, good mechanical strength, outstanding corrosion as well as fission product retention ability5–9. In these applications, carbide materials are exposed to different kinds of radiation environment, i.e., electron10, neutron11 and ion12 irradiation. Consequently, atomic defects, lattice disorder, and even structural amorphization are induced, and their mechanical properties and performances may be affected significantly. For example, radiation damage accumulation leads to a significant decrease in the bulk and Young’s moduli of 3C-SiC by 23% and 29%, respectively13. Therefore, it is of crucial importance to investigate the phase stability and the effect of point defects on the thermo-physical properties of carbides.

In the past decades, the radiation damage effect of 3C-SiC has been widely studied. Inui et al. investigated the electron irradiation-induced crystalline-to-amorphous (C-A) transition of 3C-SiC as a function of irradiation temperature employing the ultra-high-voltage electron microscopy, and they found that C-A transition can be induced at temperatures below 340 K10. The dose of electrons required for the C-A transition is essentially constant at temperatures below 250 K10. Snead et al. reported that under neutron irradiation 3C-SiC could be amorphized, and the swelling of 3C-SiC increased with the increasing neutron dose until it was saturated at the temperature region between 423 and 1073 K11. Weber et al. investigated the C-A transition of 3C-SiC using high-voltage electron microscopy with 1.5 MeV Xe+ ions over the temperature range from 40 to 550 K, and they found that the samples completely amorphized at 0.34 displacement per atom (dpa) at 0 K12. Recently, ZrC and TiC have been proposed to be promising alternatives to SiC due to their higher thermal conductivities at high temperatures and stronger tolerance to irradiation-induced-amorphization. Pellegrino et al. carried out experimental studies of the responses of SiC, TiC and ZrC to 1.2 MeV Au+ irradiation at room temperature, and found that SiC was amorphized at low Au+ fluences, whereas TiC and ZrC maintained their crystalline structure at higher Au+ fluences8. In our previous studies, an ab initio molecular dynamics simulation of low energy radiation responses of ZrC, TiC and SiC has been performed, and it was shown that carbon displacements are dominant in the cascade events and carbon disorder occurs more easily in SiC than ZrC and TiC, which may be responsible

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for the C-A transition of SiC under irradiation. The stronger radiation tolerance of ZrC and TiC than SiC can be ascribed to their different electronic structures, i.e., the $<$Ti-C$>$ and $<$Zr-C$>$ bonds are a mixture of covalent, metallic, and ionic character, whereas the $<$Si-C$>$ bond is mainly covalent.

In the meantime, researchers have paid attention to the effect of radiation damage on the mechanical properties of carbide materials. Gao et al. have employed the molecular dynamics (MD) simulation to investigate the accumulation of radiation damage of 3C-SiC due to the 10 keV Si displacement cascades and analyzed the changes in elastic constants and bulk modulus as the function of dose. They proposed that point defects and small clusters may contribute more significantly to the changes in mechanical properties than topological disorder. In their studies, the classical Tersoff-type potentials were employed and the electronic effects were not modeled. Xi et al. investigated the effect of various point defects on the volume swelling and elastic modulus of SiC employing the MD method, and reported that the Young’s modulus of SiC increased with the existence of C$_{\text{si}}$ (carbon occupying the silicon lattice site) antisite defect, while other kinds of point defects had negative influences on the change of Young’s modulus. Li et al. carried out MD simulation of the thermal properties of SiC containing carbon and silicon vacancy defects, and found that the thermal conductivity decreased pronouncedly at high concentration of carbon or silicon vacancy defect, i.e., 0.5% 25. As for the transition metal carbides, the investigations of how point defects affect the mechanical and thermal properties are very few. Dridi et al. employed the first-principle calculations to study the effect of vacancies on the structural properties in substoichiometric TiC$_{x}$ (x = 0.25, 0.5 and 0.75) and found that the bulk modulus decreased with the increasing concentration of carbon vacancy 26. Wang et al. compared the mechanical properties of TiC and TiC$_{0.25}$N$_{0.75}$ by using the first-principles calculations, and they proposed that the introduction of nitrogen significantly increased the bulk, shear and Young’s moduli of TiC. Obviously, the presence of point defects has non-negligible effects on the thermo-physical properties of carbides.

In the literature, it has been reported that under radiation environment the created defects in MC (M = Si, Ti or Zr) carbides are mainly vacancy, interstitial and antisite defects. Thus far, it is still not clear to what degree the existence of these point defects will affect the mechanical properties of carbide compounds. Theoretically, there still lacks a systematic understanding of the thermo-physical properties of defective ZrC, TiC and SiC. In order to better understand the behaviors of carbides and improve their performance under radiation environment, it is of vital importance to perform a detailed and in-depth investigation of the mechanical and thermal properties of the MC carbides. In this study, we employed first-principles calculations based on the density functional theory to investigate the stability of different kinds of point defects, including vacancy, interstitial and antisite defects. The geometrical configurations of SiC and TM C (TM = Zr and Ti), as well as the considered point defects, are illustrated in Fig. 1(a) and (b). The computational details are described in the Method section. Based on the optimized structures, the elastic constant, elastic modulus, ductility, Debye temperature and thermal conductivity of ideal and defective carbides are all predicted. The presented results provide an atomic-level insight into the effect of point defects on the mechanical and thermal properties of these carbides, and will be useful for promoting further experimental and theoretical investigations to enhance the mechanical stability of carbide materials under irradiation.

**Results and Discussion**

**Lattice parameters and formation enthalpies for ZrC, TiC and SiC.** The lattice constants for bulk ZrC, TiC and SiC are calculated and summarized in Table 1, along with the available theoretical and experimental results. Our calculated lattice constants of 4.67 Å for ZrC, 4.29 Å for TiC and 4.34 Å for SiC are shown to be in excellent agreement with the theoretical and experimental results. The formation enthalpies for carbides are obtained by $\Delta H = \mu_A^{\text{bulk}} + \mu_B^{\text{bulk}} - \mu_A^{\text{bulk}} + \mu_B^{\text{bulk}}$. The $\mu_A^{\text{bulk}}$ and $\mu_B^{\text{bulk}}$ are chemical potentials of bulk A and B, respectively. Our calculated formation enthalpy of ZrC is 1.77 eV/atom, which is comparable with the theoretical value of 1.89 eV/atom and experimental value of 1.92 eV/atom. For the formation enthalpy of TiC, our calculated value of 1.74 eV/atom is slightly smaller than the theoretical result of 1.88 eV/atom and experimental data of 1.92 eV/atom. For SiC, our calculated result of 0.56 eV/atom is much smaller than the experimental value of 1.19 eV/atom, whereas it is comparable with the theoretical result of 0.67 eV/atom. It is noted that the formation enthalpy of SiC is remarkably smaller than that of ZrC and TiC, indicating that the bonding of SiC is weaker than that of ZrC and TiC and they may exhibit different mechanical stability under irradiation.

**The defect formation energies for ZrC, TiC and SiC.** To investigate the stability of point defects, we calculated the defect formation energies based on the optimized structures. For MC (M = Si, Zr and Ti) carbides, the defect formation energy ($E_f$) is calculated by $E_f = E_{\text{def}} - E_{\text{undef}} + \sum \Delta n \mu_i$. Here, $E_{\text{def}}$ is the total energy of defective simulation cell after relaxation, $E_{\text{undef}}$ is the total energy of the ideal supercell, $\Delta n$ is the change in the number of species ($i =$ Zr, Ti, Si, or C) and $\mu_i$ is the chemical potential of species $i$, which is defined as the total energy of its bulk state. The defect formation energies are presented and compared with other theoretical results in Table 2. For ZrC, our calculated defect formation energies are generally in good agreement with the ab initio calculations of Kim et al., with an exception of the carbon and zirconium interstitials occupying the tetrahedral site. The formation energies of 3.26 eV for C interstitial and 8.01 eV for Zr interstitial are much smaller than the respective values of 3.82 and 8.72 eV in the study of Kim et al. This is mainly due to the fact that the Zr (or C) interstitial occupies the tetrahedral site that is surrounded by four Zr (or C) in our study, whereas the tetrahedral Zr (or C) are four-coordinated with two Zr atoms and two C atoms in Kim’s study. Among the point defects, the $V_C$ (carbon vacancy) defect has the lowest formation energy and the $C_{\text{si}}$ antisite (carbon occupying the zirconium lattice site) defect is the most difficult to form. As compared with ZrC, the defect formation energies in TiC are generally smaller, except the C tetrahedral interstitial defect, whereas the relative stability of the defects in both carbides shows very similar character. As for SiC, our calculated defect formation energies are generally...
Figure 1. Illustration of schematic view of defects in (a) SiC and (b) TMC \((\text{TM} = \text{Zr and Ti})\). \(V_X \) \((X = \text{C, Si, Zr or Ti})\): X vacancy; \(X_t \) \((X = \text{C, Si, Zr or Ti})\): X interstitial occupying the tetrahedral site; \(X_Y \) \((X, Y = \text{C, Si, Zr or Ti})\): X occupying the Y lattice site.

Table 1. The calculated lattice constants \(a_0\) and formation enthalpies \(\Delta H\) for ZrC, TiC and SiC. \(^a\)Ref. 6. \(^b\)Ref. 22. \(^c\)Ref. 24. \(^d\)Ref. 21. \(^e\)Ref. 26. \(^f\)Ref. 25.
Comparing the defect formation energies in these three carbides, we find that the $V_C$ defect is the most preferable in ZrC and TiC, as indicated by the lowest formation energies, while in SiC the $C_{Si}$ antisite defect is slightly more favorable than the $V_C$, and the stability of SiC antisite is comparable. These results suggest that antisite defects are relatively more easily to form in SiC than TMCs. However, both the carbon vacancy and interstitial defects are more difficult to form in SiC, since the corresponding formation energies in this compound are much higher than those in TiC and ZrC.

In order to consider the effect of chemical environment on the defect formation energies ($E_f$), we further calculate them by ref. 23

\[
E_f = E_{def} - \frac{1}{2}(n_M + n_C)\mu_{\text{bulk}}^{M} - \frac{1}{2}(n_M - n_C)(\mu_{\text{bulk}}^{M} - \mu_{\text{bulk}}^{C}) - \frac{1}{2}(n_M - n_C)\Delta\mu
\]

and

\[
\Delta\mu = (\mu_{M} - \mu_{C}) - (\mu_{M}^{\text{bulk}} - \mu_{C}^{\text{bulk}}).
\]

Table 2. The defect formation energies (eV) for MC (M = Zr, Ti and Si). $V_X$ ($X = C, Si, Zr$ or Ti): X vacancy; $X_t$ ($X = C, Si, Zr$ or Ti): X interstitial occupying the tetrahedral site; $X_Y$ ($X, Y = C, Si, Zr$ or Ti): X occupying the $Y$ lattice site. aRef. 28. bRef. 30. cRef. 29. dRef. 31.

| Defect type | Defect formation energy |
|-------------|-------------------------|
| **ZrC** | |
| $V_C$ | $1.08$ | $0.93^a$ |
| $V_{Zr}$ | $8.98$ | $8.83^a$ |
| $C_t$ | $3.26$ | $3.82^a$ |
| $Zr_t$ | $8.01$ | $8.72^a$ |
| $C_{Zr}$ | $13.28$ | $13.00^a$ |
| $Zr_{C}$ | $9.56$ | $9.56^a$ |
| **TiC** | |
| $V_C$ | $0.80$ |  |
| $V_{Ti}$ | $7.03$ |  |
| $C_t$ | $3.59$ |  |
| $Ti_t$ | $7.01$ |  |
| $C_{Ti}$ | $12.83$ |  |
| $Ti_{C}$ | $9.22$ |  |
| **SiC** | |
| $V_C$ | $3.64$ | $3.74^a$ $3.63^a$ |
| $V_{Si}$ | $8.44$ | $8.38^a$ $7.48^a$ |
| $C_t$ | $6.34$ | $5.84^a$ |
| $Si_t$ | $7.58$ | $7.02^a$ $7.04^a$ |
| $C_{Si}$ | $3.56$ | $3.28^a$ $3.48^a$ |
| $Si_{C}$ | $3.81$ | $4.43^a$ $4.02^a$ |

The elastic constants and elastic moduli for ideal and defective carbides. The elastic constants ($C_{ij}$) determine the response of the crystal to external forces, and provide important information about the
stability, stiffness and hardness of materials. For cubic systems, there are three independent elastic constants, i.e., $C_{11}$, $C_{12}$ and $C_{44}$, where $C_{11}$ represents the uniaxial deformation along the [001] direction, $C_{12}$ is the pure shear stress at the (110) crystal plane along the [110] direction and $C_{44}$ is a pure shear deformation on the (100) crystal plane. The calculated elastic constants for ideal carbides are summarized in Table 3, along with the theoretical and experimental values for comparison. The calculated results of $C_{11}$ = 460.2 GPa, $C_{12}$ = 118.1 GPa, $C_{44}$ = 138.9 GPa for ZrC, $C_{11}$ = 497.5 GPa, $C_{12}$ = 143.7 GPa, $C_{44}$ = 143.9 GPa for TiC, are generally comparable with the experimental results and other theoretical results. As for SiC, $C_{11}$, $C_{12}$ and $C_{44}$ are calculated to be 383.3, 125.2 and 239.6 GPa, respectively, which agree well with the theoretical and experimental values. It is noted that the $C_{11}$ of SiC is 76.9 and 114.2 GPa smaller than that of ZrC and TiC, respectively, whereas the $C_{44}$ of SiC is 100.7 GPa larger than ZrC and 95.7 GPa larger than TiC. Obviously, the resistance to uniaxial deformation

**Figure 2.** The defect formation energies as a function of chemical potential difference ($\Delta \mu$) in (a) ZrC; (b) TiC; (c) SiC. The $\Delta H$ and $-\Delta H$ correspond to M-rich and C-rich conditions, respectively. $V_X$ (X = C, Si, Zr or Ti): X vacancy; $I_X$ (X = C, Si, Zr or Ti): X interstitial occupying the tetrahedral site; $X_Y$ (X, Y = C, Si, Zr or Ti): X occupying the Y lattice site.
along the [001] direction and shear deformation on the (100) plane for SiC is distinct from that for ZrC and TiC, and this may cause different mechanical and between SiC and TMCs.

Based on the optimized structures, the elastic constants for defective ZrC, TiC and SiC are calculated and summarized in Table 4. As compared with the pristine states, the C44 values of ZrC and TiC containing TM C antisite defects are reduced considerably, i.e., ~38%. The existence of TM C antisite defects also decreases the C12 values by 16.8% and 14.9% for ZrC and TiC, respectively. On the other hand, the TM interstitial defects decrease the C11 of ZrC and TiC by 14.9% and 12.9%, respectively, and increase the C44 of TiC by 9.6%. As the most favorable defect in ZrC and TiC, the V C defect decreases the C12 of ZrC and TiC by 9% and 10%, respectively. Generally, the TM C antisite and TM t interstitial defects, which are not preferable for TMC under irradiation, have more significant effects on the elastic constants, and the dominant VC defect has smaller influences. The situation in SiC is found to be very different. In this carbide, the reduction in the C44 value by the dominant V C defect is as high as 65.8%. The decrease of 12% in C11 caused by the V C defect is also not negligible. Besides, the V Si and Si t decrease the C44 significantly, i.e., 22% and 30%, respectively. As for the C Si and SiC antisite defects, the influences are relatively much smaller. Obviously, the defects of VC, V Si and Si t affect the elastic constants of SiC remarkably. These results suggest that the existence of the TM C antisite and TM t interstitial defects in TMC carbides, and the VC, V Si and Si t defects in SiC generally weakens the resistance to uniaxial and shear deformation.

The bulk, shear and Young’s moduli can be estimated using Voigt-Reuss-Hill (VRH) approximation, which is an average of the lower bound of Voigt and upper bound of Reuss, and can provide a good estimation of the mechanical properties from the elastic constants. The elastic moduli and Poisson’s ratio are defined as follows:

\[
B = \frac{1}{3}(C_{11} + 2C_{12}),
\]

(3)

\[
G_V = \frac{1}{5}(C_{11} - C_{12} + 3C_{44}).
\]

(4)

\[
G_R = \frac{5(C_{11} - C_{12})C_{44}}{4C_{44} + 3(C_{11} - C_{12})}.
\]

(5)

\[
G_{VRH} = \frac{1}{2}(G_V + G_R).
\]

(6)

\[
E = \frac{9B_{VRH}G_{VRH}}{(3B_{VRH} + G_{VRH})},
\]

(7)

and

\[
\sigma = \frac{(3B_{VRH} - 2G_{VRH})}{[2(3B_{VRH} + G_{VRH})]}.\]

(8)

Here, G_v, G_R and G_{VRH} are the shear modulus calculated by Voigt, Reuss and Voigt-Reuss-Hill approximation, respectively, B is the bulk modulus, E is the Young’s modulus, and \( \sigma \) is the Poisson’s ratio. Our calculated elastic moduli for ideal carbides together with the available theoretical and experimental results are summarized in Table 3. For ZrC, our calculated results are \( B = 232.2 \) GPa, \( E = 372.3 \) GPa and \( G = 150.9 \) GPa. In the literature, Yang et al. employed the similar method and determined the elastic moduli of ZrC to be 235, 400 and 164 GPa for B, E and G, respectively\(^{38}\), which are comparable with our results. Liu et al. carried out DFT calculations with CASTEP code\(^{39}\) and ultrasoft pseudopotentials\(^{40}\), and also obtained similar results, i.e., \( B = 217.5 \) GPa,
tetrahedral site; XY (X, Y = C, Si, Zr or Ti): X interstitial occupying the tetrahedral site; X Y (X, Y = C, Si, Zr or Ti): X occupying the Y lattice site.

Table 4. The elastic constants (GPa) for ideal and defective MC (M = Zr, Ti and Si). VX (X = C, Si, Zr or Ti): X vacancy; X Y (X = C, Si, Zr or Ti): X interstitial occupying the tetrahedral site; X Y (X, Y = C, Si, Zr or Ti): X occupying the Y lattice site.

| Table 4 | Table 5. The bulk modulus B (GPa), Young’s modulus E (GPa), shear modulus G (GPa) for ideal and defective MC (M = Zr, Ti and Si), along with the relative change of the bulk modulus (ΔB), Young’s modulus (ΔE) and shear modulus (ΔG). VX (X = C, Si, Zr or Ti): X vacancy; X Y (X = C, Si, Zr or Ti): X interstitial occupying the tetrahedral site; X Y (X, Y = C, Si, Zr or Ti): X occupying the Y lattice site. |

| ZrC | | Ideal | Vc | Vm | C11 | C12 | C13 | M1 | M2 | Cm | Mc |
|---|---|---|---|---|---|---|---|---|---|---|---|
| B | 232.2 | 224.9 | 222.0 | 230.7 | 212.9 | 225.1 | 214.3 |
| ΔB (%) | −3.1 | −4.3 | −0.6 | −8.3 | −3.1 | −7.7 |
| E | 372.2 | 380.1 | 355.7 | 375.9 | 341.5 | 364.6 | 292.2 |
| ΔE (%) | 2.2 | −4.4 | 1.0 | −8.3 | −2.0 | −21.5 |
| G | 150.9 | 155.9 | 144.2 | 152.9 | 138.5 | 148.2 | 114.8 |
| ΔG (%) | 3.3 | −4.5 | 1.3 | −8.2 | −1.8 | −24 |
| TiC | | | | | | | | | | | |
| B | 261.6 | 254.1 | 251.9 | 261.3 | 244.4 | 254.6 | 246.5 |
| ΔB (%) | −2.9 | −3.7 | −0.1 | −6.6 | −2.7 | −5.8 |
| E | 391.0 | 411.2 | 381.8 | 410.4 | 376.0 | 398.6 | 308.8 |
| ΔE (%) | 5.0 | −2.4 | 4.9 | −3.8 | 1.9 | −21 |
| G | 156.3 | 167.1 | 153.0 | 165.7 | 151.2 | 160.8 | 119.6 |
| ΔG (%) | 7.0 | −2.1 | 6.0 | −3.3 | 2.9 | −23.5 |
| SiC | | | | | | | | | | | |
| B | 211.3 | 200.5 | 190.4 | 206.1 | 188.7 | 213.7 | 185.0 |
| ΔB (%) | −5.1 | −9.9 | −2.4 | −10.7 | 1.2 | −12.4 |
| E | 432.9 | 233.9 | 351.2 | 398.9 | 342.1 | 438.6 | 412.7 |
| ΔE (%) | −46 | −18.9 | −7.8 | −21 | 1.3 | −4.7 |
| G | 186.9 | 89.6 | 147.3 | 169.5 | 142.8 | 189.4 | 177.6 |
| ΔG (%) | −52.1 | −21.2 | −9.3 | −23.6 | 1.3 | −5.0 |

As for TiC, our calculated bulk, Young’s and shear moduli are 261.6, 391 and 186.9 GPa, respectively, which are in good agreement with the study of Liu et al.61, where the same code and similar computational parameters have been employed. Comparing our results with the calculations of Liu et al.61, we find that their values of B = 253 GPa, G = 481 GPa and E = 205 GPa differ a lot from our results. The large discrepancy in the Young’s and shear moduli between Liu’s study and this work as well as the work of Lu et al. is probably due to the difference in the force convergence criteria. In this work and Lu’s study, the convergence criteria for force is set to be $1 \times 10^{-5}$ eV/Å and $1 \times 10^{-6}$ eV/Å, respectively, while in Liu’s study the criteria is only $1 \times 10^{-7}$ eV/Å. For SiC, the bulk, Young’s and shear moduli are calculated to be 211.3, 432.9 and 186.9 GPa, respectively, which are in reasonable agreement with the experimental17 and theoretical18 results.

The elastic moduli for defective carbides are summarized in Table 5, along with the relative change of respective elastic modulus. As defects are introduced into ZrC, we find that the ZrC antisite defect has a remarkably negative effect on the Young’s and shear moduli, which decrease from 372.2 to 292.1 GPa and from 156.3 to 119.6 GPa, respectively. The bulk modulus is also decreased by 7.7% by the presence of ZrC antisite defect. Another defect that influences the elastic moduli relatively a lot is the Zr defect, which reduces the bulk, Young’s and shear moduli by about 8.3%. As for the Vc, VZr, Cc and CZr defects, the influences are much smaller and even negligible in some cases. In TiC, the most significant change is found to be the TiC antisite defect, for which the decreases are as large as 21% for Young’s modulus and 23.5% for shear modulus. The Ti and TiC defects also decrease the bulk modulus by 6.6% and 5.8%, respectively. It is noticeable that the carbon vacancy and interstitial
defects, which are more favorable than other defects under irradiation, have positive effects on the shear modulus, although the effect is not significant. In SiC, the influences of point defect on the elastic moduli are also generally negative. The most pronounced change is found for SiC with VC defect, for which the Young's modulus of 234 GPa and shear modulus of 89.6 GPa are remarkably smaller than the respective values of 433 GPa and 187 GPa for the ideal state. The silicon vacancy and interstitial defects also affect the elastic moduli largely, which cause the bulk, Young's and shear modulus to decrease by 9.9-10.7%, 18.9-21% and 21.2-23.6%, respectively. On the other hand, the SiC antisite defect also leads to a reduction of 12.4% in the bulk modulus.

The variation of the elastic moduli for the ideal and defective carbides is illustrated in Fig. 3. It is noted that the bulk moduli for defective SiC are generally smaller than those for defective ZrC and TiC. As for the shear and Young's moduli, the most significant changes are found for SiC with VC defect and TMCs with TM_C antisite.
As shown in Table 6, the ratios are determined to be 0.23 for ZrC, 0.25 for TiC and 0.16 for SiC, respectively. These results indicate that the ZrC with ZrC antisite defect is more ductile than the ideal state, and the ZrC with VC defect is relatively more brittle. As for TiC, the B/G ratio is 1.67, which is larger than the theoretical value of 1.22, and the experimental data of 1.33. Our calculated bulk modulus of 261.6 GPa is comparable with Liu's result of 205 GPa, whereas large discrepancy exist between Liu's overestimated shear modulus of 205 GPa and our shear modulus of 156.3 GPa, which leads to the different B/G ratios. It is noted that the B/G ratios for defective TiC with V C defect is considerably larger. Also, the Cauchy pressures for the defective TiC are smaller than the ideal state except TiC antisite defect. These results suggest that the presence of TiC antisite defect results in better ductility. In the case of SiC, the B/G ratio of 1.13 agrees well with the theoretical and experimental values of 1.17. It is noted that B/G ratios for defective SiC are generally larger than the value of 1.13, with an exception of C Si defect. Especially, the SiC with V C defect exhibits a much larger value of 2.24. Obviously, the introduction of point defects in SiC generally enhances its ductility, which can also be confirmed by the calculated results of Cauchy pressure. The defective ZrC and TiC generally exhibit larger B/G ratio and Cauchy pressure than defective SiC (except the V C state). Particularly, the Si, and C Si antisite defective states, which dominate in SiC under irradiation, are more brittle than defective ZrC and TiC. These results demonstrate that when these three carbides are exposed to radiation environment, the ZrC and TiC generally have better ductility than SiC.

As is well known, the Poisson's ratio (σ) can be regarded as an indicator to measure the degree of directionality of bonds. The value of σ is about 0.1 for strongly covalent crystals, whereas it is greater than or equal to 0.25 for ionic materials. As shown in Table 6, the ratios are determined to be 0.23 for ZrC, 0.25 for TiC and 0.16 for SiC, which are consistent with the experimental and other theoretical results. It is noted that the Poisson's ratio for SiC is smaller than that of ZrC and TiC, meaning that the Si-C bond is more covalent than the Si-C bond in ZrC and TiC.

### Table 6. The B/G ratio, Cauchy pressure C.P (GPa) and Poisson's ratio (σ) for ideal and defective MC (M = Zr, Ti and Si). V C (X = C, Si, Zr or Ti): X vacancy; X t (X = C, Si, Zr or Ti): X interstitial occupying the tetrahedral site; X Y (X = C, Si, Zr or Ti): X occupying the Y lattice site.

|       | Ideal  | V C | V M | C t | M t | M M | M C |
|-------|--------|-----|-----|-----|-----|-----|-----|
| ZrC   | 1.54   | 1.44| 1.54| 1.51| 1.54| 1.52| 1.87|
|       | 1.45±1.31 |   |   |   |   |   |   |
| C.P   | −20.8  | −36.3| −19.9| −25.7| −17.9| −23.2| 11.9|
| σ     | 0.23   | 0.22| 0.23| 0.23| 0.23| 0.23| 0.27|
|       | 0.19±0.19 |   |   |   |   |   |   |
| TiC   | 1.67   | 1.52| 1.65| 1.58| 1.62| 1.58| 2.06|
|       | 1.22±1.33 |   |   |   |   |   |   |
| C.P   | −0.19  | −25.7| −4.8| −15.8| −7.9| −13.7| 34.1|
| σ     | 0.25   | 0.23| 0.25| 0.24| 0.24| 0.24| 0.29|
|       | 0.18±0.20 |   |   |   |   |   |   |
| SiC   | 1.13   | 2.24| 1.29| 1.22| 1.32| 1.13| 1.15|
|       | 1.17±1.17 |   |   |   |   |   |   |
| C.P   | −114.4 | 50.2| −65.1| −88.2| −53.9| −115.4| −104.7|
| σ     | 0.16   | 0.31| 0.19| 0.18| 0.20| 0.16| 0.16|
|       | 0.17±0.16 |   |   |   |   |   |   |
This is consistent with our previous calculations, which demonstrated that the nature of Si-C is covalent, while the Ti-C and Zr-C bands are a mixture of covalent, ionic and metallic bands.

For ZrC and TiC, it is shown that the $\sigma$ values for defective states are generally comparable with the ideal states. One exception is the TMC with TMC antisite defects, for which the $\sigma$ values are much larger and the TM-C bonds are more ionic. As for SiC, the $\sigma$ values for SiC and CSi antisite defects are comparable with the ideal state, and other defective states have larger $\sigma$ values, particularly the SiC with V C defect, indicating that the vacancy and interstitial defects reduce the covalency of the Si-C bond. Comparing the $\sigma$ values for defective ZrC, TiC and SiC, we find that the defective ZrC and TiC generally have larger Poisson’s ratios, except for SiC with the VC. These results suggest that the TM-C bonds are less covalent than the Si-C bond. Since the defective ZrC and TiC are more ductile than SiC, we propose that the better ductility of ZrC and TiC may be resulted from the less covalency of the TM-C bonds.

The thermodynamic properties of pristine and defective carbides. The Debye temperature is often used to characterize many properties of materials, such as thermal vibration of atoms, heat capacity, and thermal expansion coefficient$^{46}$. It can be calculated by ref. $^{47}$

$$\Theta_D = \frac{\hbar}{k} \left( \frac{3n}{4\pi} \left[ \frac{N_p\rho}{M} \right] \right)^{\frac{1}{3}} \nu_m,$$

(9)

$$\nu_m = \left[ \frac{2}{3} \left( \frac{1}{\nu_s} + \frac{1}{\nu_l} \right) \right]^\frac{1}{2},$$

(10)

$$\nu_l = \sqrt{\frac{B + 4/3G}{\rho}}$$

(11)

and

$$\nu_s = \sqrt{\frac{G}{\rho}}.$$  

(12)

Table 7. The average sound wave velocity $v_m$ (m/s), Debye temperature $\Theta_D$ (K), phonon thermal conductivity $\kappa_p$ (W/mK) and electronic thermal conductivity $\kappa_e$ (W/mK) for ideal and defective MC (M = Zr, Ti and Si). VX (X = C, Si, Zr or Ti): X vacancy; Xt (X = C, Si, Zr or Ti): X interstitial occupying the tetrahedral site; XY (X, Y = C, Si, Zr or Ti): X occupying the Y lattice site. Note: *experimental result. $^6$Ref. 6. $^5$Ref. 51. $^7$Ref. 48. $^8$Ref. 49. $^9$Ref. 44. $^{10}$Ref. 50.

<Zr-C> and <Ti-C>. This is consistent with our previous calculations, which demonstrated that the nature of <Si-C> is covalent, while the <Ti-C> and <Zr-C> bands are a mixture of covalent, ionic and metallic bands. For ZrC and TiC, it is shown that the $\sigma$ values for defective states are generally comparable with the ideal states. One exception is the TMC with TM$_4$ antisite defects, for which the $\sigma$ values are much larger and the <TM-C> bonds are more ionic. As for SiC, the $\sigma$ values for Si$_4$ and C$_4$ antisite defects are comparable with the ideal state, and other defective states have larger $\sigma$ values, particularly the SiC with V$_{C}$ defect, indicating that the vacancy and interstitial defects reduce the covalency of the <Si-C> bond. Comparing the $\sigma$ values for defective ZrC, TiC and SiC, we find that the defective ZrC and TiC generally have larger Poisson’s ratios, except for SiC with the V$_{C}$. These results suggest that the <TM-C> bonds are less covalent than the <Si-C> bond. Since the defective ZrC and TiC are more ductile than SiC, we propose that the better ductility of ZrC and TiC may be resulted from the less covalency of the <TM-C> bonds.
Here, $\Theta_D$ is the Debye temperature, $h$ and $k$ are the Planck’s and Boltzmann’s constant, respectively, $n$ is the number of atoms per unit cell, $N_A$ is the Avogadro’s number, $M$ is the unit-cell molecular weight and $\rho$ is the density. In the equations (10)–(12), $v_\text{L}$ and $v_\text{S}$ are the average sound wave velocity, longitudinal sound wave velocity and shear sound wave velocity, respectively. The calculated average sound wave velocity and Debye temperature for pristine and defective carbides are summarized in Table 7, together with the available experimental48–50 and theoretical44,45 results. It is noted that the ZrC_2 and TiC antisite defects have the most pronounced negative effects on the average sound wave velocity, as indicated by the decrease from 5316.6 to 4657.7 m/s for ZrC and from 6277.7 to 5508.1 m/s for TiC. As for SiC, the most significant change is found for the VC defect, for which there is a sharp decrease in the average sound wave velocity from 1146.3 to 807.2 m/s.

The Debye temperatures are determined to be 672.6 K for ZrC and 863.3 K for TiC, which are comparable with the theoretical52,53 and experimental48,49 results. It is noted that the ZrC_2 and TiC antisite defects cause a reduction of 83.3 and 104.5 K in the Debye temperature of ZrC and TiC, respectively. As for other defects, the influences are minor and even negligible in some cases. For SiC, the calculated Debye temperature is 1146.3 K, which compares well with the theoretical value of 1111 K46 and experimental value of 1123 K50. The most pronounced change is found for SiC with VC defect, for which the Debye temperature of 807.2 K is remarkably smaller than the 1146.3 K for the ideal state. The VSi and Si defects also affect the Debye temperature largely, which cause it to decrease to 1020.1 and 1006.2 K, respectively. Generally, the material with lower Debye temperature has weaker chemical bonding and larger expansion coefficient. Comparing the Debye temperature for pristine and defective carbides, we find that the Debye temperatures of the ideal and defective SiC are generally larger than those of transition metal carbides (except the VC defective state), suggesting that the SiC will have smaller thermal expansion coefficient. The carbide materials, which are used as fuel-cladding and structural materials in nuclear reactors, need to satisfy the criterion of small thermal expansion to prevent coating failure. The ZrC and TiC, with better physical and thermal properties such as larger bulk moduli and better ductility, are promising alternatives to SiC. However, the lower Debye temperature for ZrC and TiC than SiC is not beneficial to their applications. It is thus necessary to improve the Debye temperature of ZrC and TiC for these applications as fuel-cladding and structural materials in nuclear reactors.

We further carry out density of state (DOS) analysis of the ideal and defective carbides. The total DOS distribution around the Fermi level for all carbides is illustrated in Fig. 4. As seen in Fig. 4, the SiC is a semiconductor while the ZrC and TiC compounds are of metallic character. It is shown that the introduction of point defects into ZrC and TiC does not change their metallic nature, and there are electrons distributing on the Fermi level of all defective states, while for SiC the defective states are still of the semiconducting character, except the VC and VSi defective states. Generally, the thermal conductivity of semiconductors and metals are mainly contributed by phonons and electrons, respectively. The minimum high-temperature phonon part of thermal conductivity can be obtained by Clarke’s model52, i.e. $\kappa_p^{\text{Clarke}} = 0.87 k M^2 \frac{2}{f} (E \frac{f}{2})^2$, and Cahill’s model53, i.e. $\kappa_p^{\text{Cahill}} = \frac{k}{2} \left( \frac{\rho N_A}{M} \right)^{1/2} (v_\text{L} + 2v_\text{S})$. Here, $k$ is the Boltzmann’s constant, $M$ is the unit-cell molecular weight, $E$ is the Young’s modulus, $\rho$ is the density, $N_A$ is the Avogadro’s number, $v_\text{L}$ and $v_\text{S}$ are the longitudinal and shear sound wave velocity, respectively. The electronic thermal conductivity for metallic state of carbides is calculated by $\kappa_e = \frac{\sigma}{W} k T$, where $L$ is the Lorenz number and $\sigma$ is the electrical conductivity. Here, the Lorenz number is taken to be $2.45 \times 10^{-8} \text{W} \text{Ω}^{-1} \text{K}^{-2}$ and the electrical conductivity is obtained from the imaginary part of the dielectric function50. The calculated phonon thermal conductivity for all carbides and electronic thermal conductivity for metallic states are all summarized in Table 7. As expected, the thermal conductivity of ZrC and TiC are mainly contributed by electrons and the contribution of phonons is nearly half of the contribution of electrons. As for SiC with VC and VSi, although electrons are distributing on the Fermi level, the contribution of electrons to the thermal conductivity is slight and the thermal conductivity is dominated by the phonons. Comparing the total thermal conductivity of all carbides, the thermal conductivity of ZrC and TiC are much larger than that of SiC, implying that under radiation environment the ZrC and TiC will exhibit superior heat conduction ability than the SiC.

**Conclusions**

In this work, a density functional theory study is performed to compare the mechanical and thermal properties of defective ZrC, TiC and SiC. The calculated defect formation energies show that the carbon vacancy is always the most preferable in ZrC and TiC, whereas in SiC the C\text{Si} antisite defect is dominant under C-rich condition and the carbon vacancy and Si\text{C} antisite defects are more favorable under Si-rich condition. It is shown that the carbon vacancy has minor effects on the elastic moduli, ductility and Debye temperature of ZrC and TiC, whereas its influence on the thermo-physical properties of SiC is significant. Generally, the defective ZrC and TiC have larger bulk modulus and smaller changes in the Young’s and shear moduli than SiC under radiation environment. Although the presence of defects decreases and increases the ductility of TMCs and SiC, respectively, the defective ZrC and TiC generally have larger B/G ratio and Cauchy pressure than defective SiC, and have better ductility. We also found that the thermal conductivity of defective ZrC and TiC are much larger than that of SiC. Meanwhile, the Debye temperatures for the defective SiC are generally larger than those for transition metal carbides, indicating that the SiC has smaller thermal expansion coefficient. As the alternatives to SiC as fuel-cladding and structural materials in nuclear reactors, the ZrC and TiC generally exhibit better mechanical and thermal properties than the SiC except the Debye temperature. It is thus necessary to improve the Debye temperature of transition metal carbides for their potential applications under irradiation.

**Methods**

All the calculations are carried out within the density functional theory framework using the projector augmented-wave method, as implemented in Vienna Ab Initio Simulation Package (VASP)56. Projector augmented-wave
pseudopotentials are used to describe the interaction between ions and electrons, and the exchange-correlation effects are treated using the generalized gradient approximation (GGA) in the Perdew-Wang parameterization. The Computations are based on a $2 \times 2 \times 2$ supercell consisting of 64 atoms with a $4 \times 4 \times 4$ k-point sampling in reciprocal space and a cutoff energy of 500 eV. The convergence criteria for total energies and forces are $10^{-5}$ eV and $10^{-5}$ eV/Å, respectively. The point defects, which are taken into account in the simulations, include vacancy, interstitial and antisite defects and the geometrical configurations of considered point defects are also illustrated in Fig. 1.

Figure 4. The total density of state distribution for ideal and defective carbide compounds. (a) ZrC, (b) TiC and (c) SiC. $E_F$ represents the Fermi level and is set to be zero.
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**Author Contributions**

H.X. and X.Z. designed the calculations. M.J. conducted the calculations and wrote the manuscript. J.Z. and Z.L. contributed the discussion and interpretation of the results. All authors discussed the results and reviewed the manuscript.

**Additional Information**

**Competing Interests:** The authors declare that they have no competing interests.

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