An IPAVSG Control Strategy for Microgrid With Multi-Parallel VSG System

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Virtual synchronous generator (VSG) is widely used in various distributed power generation systems due to great simulated inertia and damping support performance. However, when the microgrid (MG) composed of multi-parallel VSG is in both grid-connected and islanded modes with various large disturbances, the control strategy with fixed parameters cannot guarantee the stable operation of the MG under all disturbances. To this end, an improved parameter-adaptive virtual synchronous generator (IPAVSG) control strategy is proposed in this paper to ensure that the virtual inertia and damping are adaptively optimized with the system operating state during the disturbance process. Therefore, the dynamic performance of the power frequency regulation and transient stability are significantly improved. Meanwhile, in order to realize the output active power of each VSG is distributed among the loads according to the ratio of its rated capacity, the active power decoupling control is designed to eliminate the influence of the virtual damping on the output active power of the VSG in islanded MG. The effectiveness and practicability of the proposed control strategy are verified through several experiments.

Keywords: virtual synchronous generator, simulated inertia and damping, large disturbances, rated capacity, active power decoupling control

1 INTRODUCTION

In recent years, distributed generation (DG) devices with clean energy such as solar energy and wind energy are widely used in many fields of production and life. The microgrid, which is composed of various distributed generation units with power converter, can be integrated into the power grid or operated in islanded mode (Liserre et al., 2010; Mojica-Nava et al., 2014; Zhao et al., 2016; Meng et al., 2019). Because of the rapid penetration of distributed generation units in power systems, a variety of serious challenges such as poor transient response performance, insufficient inertia and damping have emerged (Weng S. et al., 2019; Tian and Peng, 2020). In order to effectively solve these problems, many reasonable control strategies by Ma et al. (2021c), Hu et al. (2021a) and Wang et al. (2021) have been introduced into interface power converters of DG units.

The droop control is a classical control strategy for distributed generation units. Through simulating the static droop characteristics of synchronous generator, the control of voltage and frequency of the MG system are realized. The DG with droop control can maintain the load voltage and frequency stability according to the droop curve. In addition, power can be reasonably distributed among parallel DG units according to their respective droop curves without external
communication (Li et al., 2021). However, the droop control strategy cannot provide inertia and damping similar to synchronous generator (SG) to inverter-interfaced distributed generation (IIDG) units (Li, 2019). Thus, when a large disturbance occurs, if additional power cannot be provided in time to balance the disturbance, the stability of the MG with the droop control strategy is extremely poor (Fang et al., 2019). Although the low-pass filter droop control strategy with equivalent virtual inertia is introduced by Eskandari et al. (2019), the adjustment range of the parameters is small, and the performance of dynamic adjustment needs to be further improved.

Compared with the droop control, the virtual synchronous generator (VSG) control strategy effectively solves the lack of inertia and damping in the MG (Liu et al., 2014; D’Arco and Suul, 2014; Ma et al., 2021a). The basic principle of VSG is to introduce an equivalent rotation equation to emulate the inertia and damping characteristics of synchronous generator (SG). And the concept of VSG is originally proposed by Beck and Hesse (2007) and Driesen and Visscher (2008). Then, the equivalent mathematical model and specific implementation method of VSG based on three-phase inverter are preliminarily studied by Zhong and Weiss (2011) and Zhong et al. (2014). Afterwards, the VSG control is applied in the control of voltage, frequency, power flow and so on (Yang et al., 2011). With further in-depth research, VSG control strategy or improved control strategy based on it are used in various types of equipment or occasions such as energy storage (Rene et al., 2009; Kong et al., 2019), doubly-fed induction generators (Hwang et al., 2017), high voltage direct current transmission (Aouini et al., 2016) and direct current MG (Wu et al., 2017).

VSG can effectively simulate the inertia and damping performance of SG well. Thus, when MG fluctuates violently, the system can alleviate the fluctuation of active power and frequency of DG units. Improving the dynamic characteristics of the MG by designing appropriate virtual inertia and damping coefficients has been demonstrated by Zhong et al. (2014) and Yang et al. (2011). At present, the research on parameter selection based on VSG control is mainly divided into two categories: one is the fixed virtual inertia and damping value represented by Kerdphol et al. (2018), Fang et al. (2018) and Soni et al. (2013), while the (Simpson-Porco et al., 2013; Hou et al., 2016; Meng et al., 2016; Li et al., 2017; Alipoor et al., 2018; Andalib et al., 2018; Wang et al., 2018) focus on the study of adaptive parameters. Obviously, compared with fixed parameter control, adaptive parameter control has a wider adjustment range, which can better cope with various disturbances in the MG. In the parameter adaptive control strategy mentioned above, the damping coefficient is not considered or fixed at zero by Andalib et al. (2018) Hou et al. (2016), Alipoor et al. (2018) and Simpson-Porco et al. (2013). Therefore, the areas and scenarios are easily limited. Theoretical analysis of virtual inertia and damping coefficients is not mentioned by Li et al. (2017), and the realization of the control process is complicated. The design principles of virtual inertia and damping are given by Wang et al. (2018). Therefore, the two key parameters change in opposite directions. However, the parameter extremums and optimal damping ratios that satisfy the stability of the system are not explained in any way. A control strategy called Bang-Bang is proposed by Meng et al. (2016). This strategy systematically analyzes the specific effects of virtual inertia and damping on power frequency, and designs the principle of parameter value accordingly. Unfortunately, the Bang-Bang control contains only two virtual inertia values, and the performance of the controller cannot be greatly improved. It is noteworthy that the vast majority of adaptive VSG strategies consider MG in grid-connected mode. However, the MG also needs to operate in islanded mode. In islanded mode, MG is impossible to establish an electrical connection with the power grid. So, the energy supply of the load and the voltage amplitude and frequency adjustment are independently completed by each DG unit (Lin et al., 2017). Once a disturbance occurs, the MG needs better inertia and damping support. Therefore, in order to effectively suppress the power-frequency oscillation of the perturbation process, the parameter-adaptive VSG control strategy needs to be considered for application to the islanded MG. In addition, another core control requirement is that the DG units connected in parallel should distribute the output active power proportionally according to their rated capacity (Huang et al., 2019; Jiang et al., 2020). Therefore, it is necessary to introduce both adaptive VSG and power equalization control in the islanded MG.

In summary, this paper proposes an improved parameter-adaptive VSG control strategy for MG that is suitable for grid-connected and islanded mode. In addition, power decoupling control strategy used in islanded MG is also taken into account. The outstanding features of the IPA VSG control strategy can be summarized as follows.

1) The IPA VSG control strategy proposed in this paper is suitable for grid-connected and islanded MG. In the two modes, the virtual inertia and damping can be optimally selected according to changes in the state of the MG transient adjustment process to improve the power frequency adjustment performance of the system. Especially at the initial moment of disturbance, the virtual inertia and damping quickly respond to larger values to suppress oscillation and fluctuation.

2) An active power proportional distribution control strategy is introduced into the islanded MG to eliminate the influence of damping on the output power of the DG units at steady state. Therefore, the output active power of each DG unit is proportional to its rated capacity.

The structure of this article is arranged as follows. Section The Basic Principle and Mathematical Model of VSG introduces the mathematical model and power controller of the VSG. Section The Transient Response Analysis of Parameter Perturbation analyzes the specific effects of virtual inertia and damping on the power and frequency transient adjustment process. Section The IPA VSG Control Strategy for MPVS presents the virtual inertia adaptive expression and power sharing control block diagram of two parallel VSGs suitable for both grid-connected and islanded mode. Section The Experimental Results analyzes
the experimental results and proves the superiority and feasibility of the control strategy proposed in this paper. Section The Conclusion summarizes the advantages and feasibility of the control strategy proposed in this paper.

2 BASIC PRINCIPLE AND MATHEMATICAL MODEL OF VSG

To facilitate the interpretation, the IIDG unit controlled by VSG strategy is referred to as a VSG in this paper. A classic control topology of VSG is shown in Figure 1. It is composed of an inverter triggered by PWM generator and an LC filter set to reduce the current and voltage ripple. Utilizing the current and voltage measurement signals from VSG terminals, the power calculation and frequency measurement could be expediently realized. In order to better investigate the control strategy of the inverter, the dynamic characteristics of DG and energy storages are omitted in this paper. Moreover, the state-of-charge of energy storages is supposed to well satisfy the system requirements. Hence, the IIDG containing energy storages can be substituted for a DC voltage source (Simpson-Porco et al., 2013).

As shown in Figure 1, the core of VSG can be separated into two parts: the active power control module and the reactive power control module. The active power control module is composed of the equivalent governor and mechanical model. The active power control module export phase angle and the reactive power control module produces voltage magnitude respectively, then the generated reference sine waves are conveyed to the PWM generator to emit trigger signals. The details of these two parts are shown in Figures 2, 3. The control system depicted in Figure 2 is suitable for both the grid-connected mode and islanded mode. Because the active power control module of the VSG should include the swing equation and the equivalent governor in both modes. The reactive power control module in Figure 3 includes voltage regulator and integrator, which can obtain the amplitude of reference voltage. The total mathematical model can be concluded as

\[
\begin{align*}
    P_m - P_e - D\omega_n (\omega - \omega_n) &= J\omega_n \frac{d\omega}{dt} \\
    Q_{ref} - K_p (U - U_n) - Q_e &= K_d \frac{dU}{dt} \\
    \delta &= \int (\omega - \omega_p) dt
\end{align*}
\]  

where \( P_m, P_e, Q_{ref}, Q_e \) are the virtual mechanical power, actual output active power, the reactive power reference and actual output reactive power, respectively. \( J \) and \( D \) represent the virtual inertia and the damping coefficient, respectively. \( U \) and \( U_n \) represent the voltage of the VSG and the reference voltage, and \( \delta \) is the phase angle of the voltage. In actual control, the output power angle \( \delta \) should be connected to the power angle balance compensator, which is shown in Figure 4, where \( \delta_i, \delta_i, \delta_i^* \) respectively represent the average output power angle of all VSGs in the system, the actual power angle of the \( i \)th VSG, and the power angle of the \( i \)th VSG after compensation. This method has been proposed well by Jiang et al. (2020) and Ma et al. (2021b). \( \omega \) and \( \omega_n \) indicate the virtual angular frequency and the reference angular frequency, respectively, and \( \Delta \omega = (\omega - \omega_n) \)

![Figure 1](image-url) | Classic topology and control block of MPVS.
is the frequency deviation. In both grid-connected state and islanded state, \( \omega_p \) represents the reference angular frequency of the PCC, and it is directly collected by the phase-locked loop. Under this operation, the smooth switching between islanded mode and connected-grid mode can be achieved (Wang et al., 2019). In order to avoid the complex iterative computation of Eq. (1), the controller is designed in the frequency domain.

Observations obtained from Figure 2 depict that \( P_m \) is composed of the active power reference \( P_{ref} \) and the output power regulated by the equivalent governor according to the frequency deviation. It could be expressed as

\[
P_m = P_{ref} - K_\omega (\omega - \omega_n)
\]  

(2)

Then, the whole process of the active power control module is calculated as

\[
P_{ref} - K_\omega (\omega - \omega_n) - P_e - D \omega_n \Delta \omega = J \omega_n \frac{d\omega}{dt}
\]  

(3)

where \( K_\omega \) is the droop coefficient of the equivalent governor.

Eqs. (1)–(3) indicate that the VSG control strategy plays a significant role in imitating the operating characteristics of SG through introducing the rotor motion equation.

### 3 TRANSIENT RESPONSE ANALYSIS OF PARAMETER PERTURBATION

Theoretically, VSG can be operated alone or in parallel. This paper aims to investigate the impact of some key parameters (virtual inertia and damping coefficient) on the frequency and active power outputs of the MG with multiple VSGs connected in parallel, and we called this system as the multi-parallel VSG system (MPVS). The structure of MPVS is depicted in Figure 1, where the VSGs are attached to a point of common coupling (PCC) through a distribution line, then the PCC is connected to the utility grid via circuit breaker (CB). Notice that the capacitor of the output LC filter can be neglected in consequence of the susceptance is inappreciable around the fundamental frequency. Thus, the VSG can be substituted with an ideal DC voltage source with a series output impedance.

For the purpose of deeper analyzing the output characteristics of the MPVS, networked power system, a universally applicable model, is selected for instance. Figure 5 depicts the equivalent model of networked power system, which contains multi-paralleled virtual synchronous generators. To simplify the model, the reactive power output is not considered in this system and these simplifications have no impact on the precision of the model (Zhong et al., 2014). According to Eqs. (1) and (3), the mathematical model of VSGi can be expressed as

\[
\begin{cases}
P_{ref} - K_\omega (\omega_i - \omega_n) - P_{ei} - D \omega_n (\omega_i - \omega_n) = J \omega_n \frac{d\omega_i}{dt} \\
\delta_i = \int (\omega_i - \omega_p) dt
\end{cases}
\]  

(4)

where \( P_{ei} \) means the active power of VSGi flowing into PCC. The relationship between the \( P_{ei} \) and the variables at PCC can be expressed as

\[
P_{ei} = \frac{3E_i U_p}{Z_i} \sin \delta_i = K_p \sin \delta_i
\]  

(5)

where \( K_p = 3E_i U_p / Z_i \), \( E_i \) and \( U_p \) represent the output voltages of the VSG \( i \) and the PCC separately. \( P_{ei} \) denotes the output active power. \( Z_i \) represents the equivalent line impedance and the output impedance. \( \sin \delta_i \) represents power angle. \( Z_L \) is the load impedance.
The small signal model of the two-parallel VSG system is derived as follows. Let

\[
\begin{align*}
\omega_i &= \omega_{i0} + \Delta \omega_i \\
\omega_p &= \omega_{p0} + \Delta \omega_p \\
\delta_i &= \delta_{i0} + \Delta \delta_i \\
P_i &= P_{i0} + \Delta P_i
\end{align*}
\]

(6)

Notice that the state variables in Eq. (6) are equivalent to the value of steady state plus a perturbation value. Since $\Delta \delta_i$ is very small, the following equations $\sin(\Delta \delta_i) = \Delta \delta_i$ and $\cos(\Delta \delta_i) \approx 1$ are satisfied. Furthermore, the second-order perturbation terms could be omitted due to the frequency deviation is comparatively small. Therefore, the small signal model of Figure 2 can be obtained as Figure 6. Then the closed loop transfer function from $\Delta P_{ref}$ to $\Delta P_i$ is obtained as

\[
\frac{\Delta P_i}{\Delta P_{ref}} = \frac{E_i U_p}{J_i \omega_i Z_i Z_s^2 + D_{pi} Z_s + E_i U_p}
\]

(7)

where $D_{pi} = K_{wi} + D_i \omega_i$.

In line with Eq. (7), the peak time $t_{p-p}$, settling time $t_{s-p}$ and overshoot $M_{p-p}$ of the step response of the active power can be expressed as follows:

\[
t_{p-p} = \frac{2n J_i \omega_i Z_i}{\sqrt{4J_i \omega_i Z_i E_i U_p - D_{pi}^2 Z_i^2}}
\]

(8)

\[
M_{p-p} = e^{-\frac{D_{pi}^2 Z_i^2}{4J_i \omega_i Z_i E_i U_p - D_{pi}^2 Z_i^2}}
\]

(9)

\[
t_{s-p} = \frac{D_{pi}}{2} \frac{Z_s}{\sqrt{J_i \omega_i E_i U_p}}
\]

(10)

The closed loop transfer function from $\Delta P_{ref}$ to $\Delta \omega_i$ can be obtained as

\[
\frac{\Delta \omega_i}{\Delta P_{ref}} = \frac{Z_s}{J_i \omega_i Z_i s^2 + D_{pi} Z_s + E_i U_p}
\]

(11)

According to Eq. (11), the influences on the step response of frequency caused by $D_{pi}$ can be indicated as:

\[
t_{p-w} = \frac{E_i U_p}{J_i \omega_i Z_s - E_i U_p}
\]

(12)

\[
M_{p-w} = \frac{E_i U_p}{\sqrt{4J_i \omega_i Z_i Z_s^2 + D_{pi} Z_s + E_i U_p}}
\]

(13)

\[
t_{s-w} = \frac{8J_i \omega_i}{D_{pi}}
\]

(14)

In line with Eq. (7) and (11), the poles, the natural oscillation angular frequency and damping ratio of the characteristic equation can be calculated as

\[
s_{1,2} = \frac{-D_{pi} Z_s \pm \sqrt{D_{pi}^2 Z_i^2 - 4J_i \omega_i Z_i E_i U_p}}{2J_i \omega_i Z_i}
\]

(15)

\[
\begin{align*}
\omega_{ni} &= \frac{K_{pi}}{J_i \omega_i} \\
\zeta_{ni} &= \frac{D_{pi}}{2} \frac{1}{\sqrt{J_i \omega_i}}
\end{align*}
\]

(16)

Eqs. (7)–(16) clearly shows that the natural oscillation angular frequency and damping ratio are determined by virtual inertia and damping coefficient. The typical indexes for the dynamic response the peak time ($t_p$), overshoot ($M$) and settling time ($t_s$) are directly associated with natural oscillation angular frequency and damping ratio, so that the dynamic responses of frequency and active power of VSG have relation to $J_i$ and $D_{pi}$. The specific reflect is summarized in Table 1. Furthermore, the transit stability is affected by the two parameters as well since the poles would be to close to the imaginary axis to arouse oscillations. In other words, when the disturbances occur, not only deteriorated
roughly similar when it changes dynamically, so the dynamic coefficient on frequency and active power dynamic responses are connected and islanded MG. This strategy is suitable for both grid-connected and islanded MG is proposed, with which the ameliorative dynamic responses of the MPVS can be achieved. Furthermore, proportional power sharing during steady operation is accomplished based on adaptively adjusting the virtual inertia and damping coefficient. Notice that the large or small virtual inertia value mentioned here is relative to the steady-state virtual inertia. Besides, considering the stability of the system, the upper and lower limits ($J_{\text{max}}$ and $J_{\text{min}}$) of the virtual inertia need to be taken into consideration, because low frequency oscillations of active power may be caused if inertia exceeds the limits. Based on the aforementioned analysis, the arc-tangent function is employed for adaptive calculation of virtual inertia. The adaptive control strategy with adjustable virtual inertia is designed as follows:

$$J_i = \begin{cases} J_o + \frac{J_{\text{max}} - J_o}{\pi/2} \arctan \left( \frac{\Delta \omega}{2M_i} \times \text{sign} \left( \frac{d\omega}{dt} \right) \right), & |\Delta \omega| > M_i \cap \Delta \omega \times \text{sign} \left( \frac{d\omega}{dt} \right) > 0 \\ J_o + \frac{J_{\text{max}} - J_{\text{min}}}{\pi/2} \arctan \left( \frac{\Delta \omega}{2M_i} \times \text{sign} \left( \frac{d\omega}{dt} \right) \right), & |\Delta \omega| > M_i \cap \Delta \omega \times \text{sign} \left( \frac{d\omega}{dt} \right) \leq 0 \\ J_o, & |\Delta \omega| \leq M_i \end{cases}$$

where $J_o$ is the steady-state virtual inertia, which is associated with the rated capacity. $M_i$ is the frequency deviation threshold set to avoid the chattering of $J_i$ during steady state. In theory, of frequency is modified. With respect to virtual inertia, in the case of large disturbances and sudden changes, within a limited value range, the smaller the virtual inertia is, the shorter the settling time becomes. In contrast, the larger the virtual inertia is, the smaller the overshoot and the longer the peak time stay, which means the firmer system holds. In order to combine these advantages, the virtual inertia should show a large value when the frequency deviates and a small one when frequency recovers (Andalib et al., 2018). Moreover, Eq. (16) shows that the damping coefficient changes accordingly with the virtual inertia. For quantitative selection of virtual inertia, the step responses of the output frequency are plotted, and shown as Figure 7. The two dashed lines represent the step responses of the output frequencies with two fixed rotational inertias $J$. Furthermore, as indicated by the expected curve (the solid one) in the picture above, if a big $J$ is selected in the rising area and a small $J$ is given in the descending area, the response time of the output frequency is decreased and the overshoot is also reduced. According to the same analysis method, the rules of the selection of virtual inertia and damping coefficient during transient process can be summarized as Table 2.

| Indexes | Frequency | Active power |
|---------|-----------|--------------|
| $J_i$   | $D_{pi}$  | $J_i$        |
| $t_{si}$| $D_{pi}$  | $D_{pi}$     |
| $M_{pi}$| $D_{pi}$  | $D_{pi}$     |

**FIGURE 7** | Step response of frequency when $J$ changes.

### 4 THE IPAVSG CONTROL STRATEGY FOR MPVS

In this section, a IPAVSG control strategy appropriate for both grid-connected and islanded MG is proposed, with which the ameliorator dynamic responses of the MPVS can be achieved through adaptively adjusting the virtual inertia and damping coefficient. Furthermore, proportional power sharing during steady operation in islanded mode is accomplished based on decoupling the coupled effect between the damping coefficient and equivalent governor droop coefficient on active power outputs.

#### 4.1 Parameter-Adaptive VSG Control Strategy

In view of above analysis, if the virtual inertia and damping coefficient are selected improperly, deteriorated oscillations with long settling time and large overshoot will be aroused. Therefore, an adaptive virtual inertia and damping control strategy is designed to adaptively adjust inertia and damping to ameliorate the dynamic responses. This strategy is suitable for both grid-connected and islanded MG.

From Table 1, the influences of virtual inertia and damping coefficient on frequency and active power dynamic responses are roughly similar when it changes dynamically, so the dynamic responses of the active power will also be improved if those
there should also be a threshold $M_i$ set for $\Delta \omega/\Delta t$, and the adaptive control for $J_i$ will be triggered only if both $|\Delta \omega| > M_i$ and $\Delta \omega/\Delta t > M_i$ are satisfied. However, whether the frequency keeps stable or not is mainly determined by $\Delta \omega$, while the sign of $\Delta \omega/\Delta t$ only represents the trend of frequency changing, and the value of $\Delta \omega$ is normally smaller than $\Delta \omega$ especially at the initial stage when disturbances occur. Therefore, to facilitate analysis, only the threshold for $\Delta \omega$ is set in this paper. In actual situations, the change of $\Delta \omega_i$ may be small, $\Delta \omega/2M_i$ is introduced in this paper to amplify the frequency fluctuation value. With the proper threshold setting, the system can effectively filter out small disturbances while keeping sensitive to large disturbances. If the trigger condition $|\Delta \omega| > M_i$ is satisfied, the virtual inertia will be adaptively changed.

The curve of the virtual inertia is depicted in Figure 8. The right half part represents the period of frequency deviating whereas the left means the period of frequency recovering. As can be seen in Figure 8, different from the bang-bang control, the adaptive control strategy designed here contributes to a continuous and broader range of virtual inertia. When the frequency deviates with the feature of $\Delta \omega \times \text{sign}(\Delta \omega/\Delta t) > 0$, the larger $\Delta \omega$ is, the larger virtual inertia correspondingly becomes, which helps to suppress the overshoot and delay the peak time of the frequency oscillation. In reverse, smaller virtual inertia is conducive to shorten the settling time and accelerate the response speed when frequency recovers. In the whole process, the application of the arc-tangent function enables the virtual inertia to be more sensitive to frequency deviation, even for the initial small $\Delta \omega$, the $J_i$ obtained from Eq. (17) is capable to be comparatively large to suppress the oscillation effectively at the initial stage of disturbances. With the further increase of the $\Delta \omega$, the $J_i$ transits to the limits smoothly without beyond it, which is favorable for ensuring the system transient stability.

In terms of the damping coefficient, according to Table 1, the adjustment of $D_i$ influences frequency and active power dynamic responses in a similar tendency (Hu et al., 2021b). The adaptive control strategy of $D_i$ is designed as

$$\zeta_i = \frac{D_i \omega_i + K_{ci}}{2} \sqrt{\frac{1}{J_0 J_{pi}}} = \text{constant}$$

Equation (18) means that during the transit process, the $J_i$ and $D_i$ are adaptively adjusted in a similar tendency and at the same time with a constant damping ratio. The upper or lower limits of virtual inertia and damping coefficient are obtained when the damping ratio is 0.7 or 1. In practice, the optimal damping ratio ($\zeta_i = 0.707$) is usually adopted for the best situation of the system. Hence, the damping ratio is kept at 0.707 in this paper to better ameliorate the dynamic responses and improve transient stability.

4.2 Active Power Proportional Distribution Control Strategy

In accordance with the above analysis, the active power outputs $P_i$ are associated with the coupled effect of primary frequency $\omega_p$ modulation and the damping characteristic in steady-state of islanded MG with MPVS. In general, the governor droop coefficient is set as $K_{ci} = S_{rat}/(0.1\% \omega_p)$, $S_{rat}$ represents the rated capacity of the $i$th virtual synchronous generator (Zhang et al., 2017), and the value of $D_i$ is supposed to prioritize the requirements of the best dynamic response. As can be seen in Figure 9, to fulfill these requirements, an active power proportional distribution control strategy is proposed to decouple the interaction between the equivalent governor droop coefficient and the damping coefficient in the conventional VSG control and eliminate the effect of $D_i$ on the active power output during steady operation in islanded MG.

When the system is running in an islanded state and remains stable, the output angular frequency of the inverter $\omega$ no longer changes. According to equation Eq. 3 and Figure 9, the active power output by VSGi and VSGj is shared in proportion to formula Eq. (19).

$$\frac{P_{ei}}{P_{ej}} = \frac{P_{refi} - K_{ai}(\omega - \omega_p)}{P_{refj} - K_{aj}(\omega - \omega_p)} = C$$

Therefore, whether the line impedance is resistive, inductive or capacitive, the active power ratio sharing is determined by $P_{ref}$, $K_a$ and $(\omega - \omega_p)$.

Compared to the conventional VSG control strategy, the principal modification is the introduction of a first-order lead-lag unit in the damping feedback loops. Then, the closed loop transfer function of $\Delta P_i$ is obtained as follows

$$\frac{\Delta P_i}{\Delta \omega_p} = \frac{K_p \times [J_0 \omega_n T_{ci} s^2 + (J_0 \omega_n + D_i T_{ci} + K_{ai} T_{ci}) s + K_{pi}]}{J_0 \omega_n T_{ci} s^2 + (J_0 \omega_n + D_i T_{ci} + K_{ai} T_{ci}) s^2 + (K_{ai} + K_p T_{ci}) s + K_{pi}}$$

$$\Delta \omega_p = \frac{J_0 \omega_n T_{ci} s^2 + (J_0 \omega_n + D_i T_{ci} + K_{ai} T_{ci}) s^2 + (K_{ai} + K_p T_{ci}) s + K_{pi}}{J_0 \omega_n T_{ci} s^2 + (J_0 \omega_n + D_i T_{ci} + K_{ai} T_{ci}) s^2}$$

| TABLE 2 | Rules of $J_i$ and $D_i$. |
|---------------------------------|---------------|---------------|
| Parameters                      | $J_i$          | $D_i$          |
| $\Delta \omega \times \text{sign}(\Delta \omega/\Delta t) > 0$ | large          | large          |
| $\Delta \omega \times \text{sign}(\Delta \omega/\Delta t) \leq 0$ | small          | small          |

**FIGURE 8** | Changing curve of virtual inertia.
Equation (20) illustrates that the active power output is only up bounded by $K_{wi}$ and the effect of $D_i$ has been eliminated during steady state. The specific implementation process of the whole control strategy is as follows.

$$S_i = \begin{cases} 1, & |\Delta \omega_i| \leq M_i \\ 0, & |\Delta \omega_i| > M_i \end{cases}$$

During steady operation, the switching state value $S_i$ remains at one and the branch included the first-order lead-lag unit is chosen to decouple the effect of $D_i$ on active power output. Subsequent to disturbances, $S_i$ changes to 0 so that the adaptive control of $J_i$ and $D_i$ will be activated. Consequently, the proportional power sharing of the MPVS during steady operation can be ensured while the dynamic responses of the system in transient process is ameliorated.

5 EXPERIMENT RESULTS

In this section, verifications of the IPAVSG control strategy are conducted through experiment results. As can be seen from Figure 10, the experimental platform contains two IIDG units operated in parallel. The corresponding experimental parameters are shown in Table 3. The parallel hard-switched PWM converters are digitally controlled by TMS28335 fixed-point DSP to implement the power and voltage control algorithm where switching frequency is 20 kHz. In practice, in order to save resource, a discrete table is created in advance. The value of $\arctan(x)$ can be directly taken from the table.

Firstly, an experiment is executed in grid-connected MG to verify the IPAVSG control strategy. The performances of the controllers to follow the power reference and maintain frequency stability are evaluated during a sudden load variation. The
TABLE 3 | Parameters of the TEST system.

| Parameters                     | Symbol | Values                  |
|--------------------------------|--------|-------------------------|
| Reference DC-bus voltage       | $U_{dc}$ | 700V                    |
| Reference AC-bus voltage       | $U_{n}$  | 380V                    |
| Reference frequency            | $f_{n}$  | 50Hz                    |
| Reference or grid angular frequency | $\omega_{ng}$ | 50Hz                 |
| Line impedance                 | $X_L$   | 0.032Ω                  |
| $R_L$                          |         | 0.2Ω                    |
| $L_f$                          |         | $3 \times 10^{-5}$H     |
| $C_f$                          |         | $15 \times 10^{-6}$F    |
| Current controller             |         | Proportional gain 0.1   |
| Voltage controller             |         | Proportional gain 280.8 |
| Integral gain                  |         | 0.2                     |
| IPAVSG                         |         |                         |
| the rated inertia              | $J_0$   | 3                       |
| maximum inertia                | $J_{\max}$ | 8                    |
| minimum inertia                | $J_{\min}$ | 0.3                |
| the rated damping coefficient  | $D_0$   | 25                      |
| maximum damping coefficient    | $D_{\max}$ | 40                   |
| minimum damping coefficient    | $D_{\min}$ | 8                   |
| droop coefficient              | $K_\omega$ | $1 \times 10^4$          |
| Stator resistance              | $R_s$   | 0.01Ω                   |
| Stator inductance              | $L_s$   | $3.56 \times 10^{-3}$H |
| Bang-Bang                      |         |                         |
| big inertia                    | $J_{\text{big}}$ | 5                   |
| small inertia                  | $J_{\text{small}}$ | 1                   |
| big damping                    | $D_{\text{big}}$ | 30                  |
| small damping                  | $D_{\text{small}}$ | 25                |
| droop coefficient              | $K_{\omega}$ | $1 \times 10^4$          |
| VSG                            |         |                         |
| inertia                        | $J$     | 3                       |
| damping                        | $D$     | 25                      |
| droop coefficient              | $K_{\omega}$ | $1 \times 10^4$          |

references of active and reactive power for each IIDG unit are assigned as 6 kW and 1 kVar. Then a 2 kW, 400 Var PCC load reduction happens at 6.4s.

The frequency and active power dynamic responses controlled by the conventional VSG and the Bang-Bang and the IPA VSG control strategies are displayed in Figures 11, 12. Similar to the previous statement, only the results of IIDG1 are displayed here because the parameters of the two IIDG units are identical. When the load decreases suddenly, the frequency deviations of the three control strategies are 0.027, 0.014 and 0.006 Hz, respectively. Besides, the active power overshoot of the three control strategies are 1120, 510 and 250 W, respectively. Obviously, the experiment results have verified that the frequency and active power deviations can be suppressed with the virtual inertia and the damping coefficient in three VSG control strategies, in which the suppression is more effective in the IPA VSG control strategy since the parameters can be adaptively adjusted.

Another experiment is executed in islanded MG. The rated capacities of the two IIDG units are 10kW and 5kW, respectively. The MG is operated steadily with PCC loads rated at 12 kW at frist. A 1.2 kW load step decrease happens at 0.5s, then reconnects to the MG at 1.3 s.

The IPA VSG control strategy in the islanded MG is supposed to not only realize the adaptive tuning of virtual inertia and damping coefficient, but also proportional active power sharing. The former experiment results have illustrated the buffer and suppression effect of virtual inertia and the damping coefficient,
6 CONCLUSION

An IPAVSG control strategy consists of adaptive virtual inertia and damping coefficient control along with decoupling control is proposed in this paper. The IPAVSG strategy can be adopted for MG with multiple IIDG units connected in parallel. The adaptive virtual inertia and damping control of IPAVSG has significantly ameliorated the dynamic responses of the MG in both grid-connected and islanded modes. Additionally, the active power outputs during steady state in islanded MG can be shared proportionally to rated capacities of IIDGs. The virtual inertia and damping coefficient of the IPAVSG control strategy can be adaptively adjusted based on the frequency responses, their proper selections are of great essentiality to the system dynamic resonances. In conclusion, the IPAVSG control strategy is of great benefit to the stability of the system.

Several experiment results in both grid-connected and islanded MG with different contingencies are conducted to validate the advantages and effectiveness of the IPAVSG control strategy. Comparisons between the conventional VSG control and Bang-Bang control are also provided in this paper, which facilitates a thorough acknowledge of these two promising control strategies for the utilization and development of renewable energy.

DATA AVAILABILITY STATEMENT

The original contributions presented in the study are included in the article/supplementary material, further inquiries can be directed to the corresponding author.

AUTHOR CONTRIBUTIONS

XS has done the main theory research work. FZ, XC, and JL conceived the project and wrote the manuscript. RW, YZ and YL designed and participated in the experiment. All authors discussed the results, read, and commented on the manuscript.

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REFERENCES

Alipoor, J., Miura, Y., and Ise, T. (2018). Stability Assessment and Optimization Methods for Microgrid with Multiple VSG Units. IEEE Trans. Smart Grid 9 (2), 1462–1471. doi:10.1109/TSG.2016.2592508

Andalib-Bin-Karim, C., Liang, X., and Zhang, H. (2018). Fuzzy-Secondary-Controller-Based Virtual Synchronous Generator Control Scheme for Interfacing Inverters of Renewable Distributed Generation in Microgrids. IEEE Trans. Ind. Appl. 54 (2), 1047–1061. doi:10.1109/TIA.2017.2773432

Aouini, R., Marinescu, B., Ben Kilani, K., and Elleuch, M. (2016). Synchronverter-Based Emulation and Control of HVDC Transmission. IEEE Trans. Power Syst. 31 (1), 278–286. doi:10.1109/tpwrs.2015.2389822

and the conventional VSG control strategy has less superiority than the Bang-Bang and IPAVSG control strategies in oscillation suppression. Hence, in this experiment, we focus on the performance comparison of Bang-Bang and IPAVSG control strategies.

The frequency and active power of the system are displayed in Figures 13, 14. To get a clearer illustration, only the frequency responses of IIDG1 are displayed. Figure 13 depicts that the frequency overshoot controlled by IPA VSG is 0.015 Hz, which is much smaller than 0.028 Hz of Bang-Bang control. And the frequency rising tendency controlled by IPA VSG is much slower than that of Bang-Bang. Therefore, the better performances in suppressing frequency dynamic response can be found in the IAPVSG control strategy. Furthermore, during steady operation, the loads connected to IIDG1 and IIDG2 of IPA VSG are 8000 and 4000 W, respectively. During load transition, the loads decrease by 800 W and 400 W, respectively. The active power decrease is even slower. By contrast, the loads supported by IIDG1 and IIDG2 of Bang-Bang are 8400 and 3600 W during steady state, then the loads reduction are 840 W and 360 W after 0.5 s. Besides, the active power decrease is slight faster. These experiment results could validate that the IAPVSG control strategy containing adaptive virtual inertia and damping control and decoupling control in islanded MG, has effective impact on ameliorating frequency and active power dynamic responses and has decoupling effect of damping coefficient on power sharing, with which the outputs could transit to a new steady state smoothly and the loads can be shared proportionally no matter before or after the load transition.
Conflict of Interest: The authors declare that the research was conducted in the absence of any commercial or financial relationships that could be construed as a potential conflict of interest.

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