Molecular gas in the bulge and ring of NGC 7331

F.P. Israel\(^1\) and F. Baas\(^1,2\)

\(^1\) Sterrewacht Leiden, P.O. Box 9513, NL 2300 RA Leiden, The Netherlands
\(^2\) Joint Astronomy Centre, 660 N. A'ohoku Pl., Hilo, Hawaii, 96720, USA

Received 6 January 1999; accepted 5 August 1999

**Abstract.** CO emission from the Sb(rs)I-II galaxy NGC 7331 has been mapped in the \(J = 2-1\) transition with a 21" beam over an area 3.5' by 1.3'. A relatively low contrast enhancement of molecular line emission occurs in a ringlike zone at a distance of approximately 3.5 kpc from the center; there is no evidence for a pronounced central hole. The ring is located at the edge of the region of rigid rotation and roughly coincides with an inhomogeneous ring of nonthermal radio continuum emission. It is well inside the radius of maximum rotational velocity.

The intensities of the 492 GHz [CI] line and various \(^{12}\)CO and \(^{13}\)CO transitions observed towards the center and two outlying positions are modelled by multiple molecular gas components: low-density gas at a kinetic temperature \(T_{\text{kin}} \approx 10\) K, and high-density gas at both \(T_{\text{kin}} \approx 10\) K and \(T_{\text{kin}} \approx 20\) K. The molecular gas must be distributed in clumpy or filamentary form. The CO-to-H\(_2\) conversion factor \(X\) applicable to the bulge is only half that applicable to the ring and beyond. The latter is still significantly lower than \(X_{\text{MilkyWay}}\). Molecular hydrogen is the dominant mass contributor to the interstellar medium in the bulge and in the ring. Far-infrared emission from dust peaks inside the ring at 100\(\mu\)m (warm dust), and in the ring at 850\(\mu\)m (colder dust). Beyond the ring, neutral atomic hydrogen is dominant. Inferred total hydrogen mass densities in the ring are about twice those in the bulge. Interstellar gas to dynamical mass ratios are of order 1% in the bulge, about 1.5% in the ring followed by a rise to 3%. The bulge gas may have originated in mass loss from bulge stars; in that case, the molecular ring is probably caused by a decrease in evacuation efficiency at the bulge outer edge.

**Key words:** Galaxies – individual (NGC 7331) – ISM – spiral – structure; Radio lines – galaxies; ISM – molecules

### Table 1. NGC 7331 parameters

| Type\(^a\) | Sb(rs)I-II |
|---|---|
| Optical Centre: | |
| R.A. (1950)\(^b\) | 22\(^h\)34\(^m\)47.7\(^s\) |
| Decl. (1950)\(^b\) | 34\(^°\)09'35" |
| Radio Centre: | |
| R.A. (1950)\(^c\) | 22\(^h\)34\(^m\)46.4\(^s\) |
| Decl. (1950)\(^c\) | 34\(^°\)09'21" |
| \(V_{\text{LSR}}\) | 831 km s\(^{-1}\) |
| Distance \(D\) | 14.3 Mpc |
| Inclination \(i\) | 74.8° |
| Position angle \(P\) | 167° |
| Luminosity \(L_B\) | \(5.0 \times 10^{10} L_{\odot}\) |
| Scale | 14.5"/kpc |

Notes to Table 1:

\(^a\) RSA (Sandage & Tammann 1987)
\(^b\) Dressel & Condon (1976)
\(^c\) Begeman (1987); Cowan et al. (1994)
\(^d\) Corresponding to \(V_{\text{hel}} = 820\) km s\(^{-1}\) (Begeman 1987)
\(^e\) Tully (1988); corresponds to \(H_\alpha = 75\) km s\(^{-1}\)
\(^f\) HI-derived parameters from Begeman (1987)

### 1. Introduction

NGC 7331 is an isolated spiral galaxy of type Sb(rs)I-II with prominent dust lanes close to its centre (Kormendy & Norman 1979; Sandage & Tammann 1987). Table 1 summarizes the relevant parameters of NGC 7331. A ringlike distribution of dust surrounding the bulge was suggested by Telesco et al. (1982). Such a distribution is also apparent in radio continuum maps (Cowan et al. 1994), but only vaguely in HI maps (Bosma 1978; Begeman 1987). A strong ring signature in CO emission was claimed by Young & Scoville (1982).

Several galaxies are thought to host a molecular ring structure (see e.g. Braine et al. 1993), such as the ring in our own Galaxy discovered by Scoville & Solomon (1975) and the one in M 31 (Stark 1979; Dame et al. 1994; Koper 1993). The latter serves to illustrate a dilemma commonly faced for the interpretation of CO maps, especially those of highly inclined galaxies where rings are most easily discerned: the conspicuous molecular structure may in fact consist of spiral arm segments that only in projection sug-
gest a ringlike structure. Two-dimensional CO mapping of NGC 7331 by von Linden et al. (1996) and Tosaki & Shioya (1997) support the latter interpretation. Although molecular rings have been identified in or claimed for other galaxies, the case of NGC 7331 is of interest because it resembles M 31 in being a large spiral galaxy of relatively early type, containing a prominent stellar bulge. It has also been claimed to have, as M 31, very little CO emission inside its molecular ring (Young & Scoville 1982; Tosaki & Shioya, 1997). NGC 7331 even resembles M 31 in its high inclination (75° and 77° respectively – Arp & Kormendy 1972, Sandage & Tammann 1987). Its radio structure is a stronger version of that of M 31 (Cowan et al. 1994). NGC 7331 also contains a clear, but patchy radio continuum ring. Inside the ring, little or no radio emission is found, except for a compact nuclear source. The luminosity of this source is 3–4 times that of Sgr A, and a thousand times stronger than the nucleus of M 31. It is associated with a nuclear X-ray source (Stockdale et al. 1998). Ringlike distributions of interstellar dust are also seen at mid-infrared (Smith 1998) and submillimeter (Blanchi et al. 1998) wavelengths, but they are not nearly as evident at the far-infrared wavelengths inbetween (Smith & Harvey 1996; Alton et al. 1998).

An unusual characteristic of NGC 7331 is the rather low $J=2–1/J=1–0$ CO transitional ratio of 0.5–0.7 reported by Braine et al. (1993) and von Linden et al. (1996). This is quite different from most other galaxies observed in CO, where the two transitions are usually of similar strength. However, such low transitional ratios have also been found for individual dark clouds in the central parts of M 31 (Allen & Lequeux 1993). These were interpreted as evidence for very cold ($T_{\text{kin}} < 5$ K) and tenuous ($n \approx 100 \text{ cm}^{-3}$) molecular clouds by Loinard et al. (1995), but Israel et al. (1998) showed that they are more likely caused by filamentary gas at temperatures $T_{\text{kin}} \approx 10$ K present at both low and high densities. Given the similarities between NGC 7331 and M 31, it is of interest to investigate whether such a state of affairs also applies to the central region of NGC 7331.

In this paper, we present a fully sampled map of NGC 7331 in the $J=2–1$ $^{12}$CO transition over an area of 1.3′ by 3.5′. In addition, we have measured the first three $^{13}$CO and $^{12}$CO transitions as well as the 492 GHz CI transition towards the central region of the galaxy, allowing us to narrow down the permitted range of the apparently unusual physical conditions in the center.

### 2. Observations

Details relevant to the observations are listed in Table 2; the system temperatures given are the means for the respective runs. Observations in the $J=1–0$ transition were obtained with the IRAM 30 m telescope in service mode, at the optical and radio centre positions respectively, separated by $\Delta \alpha = 13.7''$, $\Delta \delta = 14.0''$. The $^{13}$CO observations were bracketed by the $^{12}$CO observations.

All other observations were carried out with the 15m James Clerk Maxwell Telescope (JCMT) on Mauna Kea (Hawaii). Up to 1993, we used a 2048 channel AOS backend covering a band of 500 MHz (650 km s$^{-1}$ at 230 GHz). After that year, the DAS digital autocorrelator system was used in bands of 500 and 750 MHz. Resulting spectra were binned to resolutions of 4 – 10 km s$^{-1}$, except for the 492 GHz CI spectrum which was binned to 18 km s$^{-1}$ on order to obtain a sufficiently high signal-to-noise ratio. Only linear baseline corrections were applied to the spectra. All spectra were scaled to a main-beam brightness temperature, $T_{mb} = T_A^* / \eta_{mb}$; relevant values for $\eta_{mb}$ are given in Table 2. Spectra are shown in Fig. 1 and summarized in Table 3. Position A (indicated in Figure 2) is that of the radio nucleus, the actual galaxy center. Along the minor axis, the beam just fills the space between the ring components. Positions B and C are close to the minor axis at deprojected radii $R = 4.5$ kpc and $R = 8.2$ kpc respectively; position B is centered on the CO ring. Because of the pronounced tilt of the galaxy, 21″ circular observing beams sample elongated ellipses in the plane of the galaxy, covering a range of 5.55 kpc in the minor axis direction. The beams covering positions B and C overlap (see Figure 2); positions A and B are essentially independent.

For the $J=2–1$ mapping observations, the integration time was typically 400 seconds per spectrum, on and off

| Transition | Date (MM/YY) | Freq (GHz) | $T_{\text{sys}}$ (K) | Beamsize $\eta_{mb}$ |
|------------|--------------|------------|----------------------|----------------------|
| $^{12}$CO  | $J=1–0$      | 07/97      | 115                  | 350                  | 21                  | 0.74 |
|            | $J=2–1$      | 11/91      | 230                  | 850                  | 21                  | 0.63 |
|            |              | 08–10/92   | 600                  | 21                  | 0.63 |
|            |              | 01/96      | 500                  | 21                  | 0.69 |
|            |              | 12/97      | 260                  | 21                  | 0.69 |
| $J=3–2$    | 05/93        | 345        | 720                  | 14                  | 0.53 |
|            | 07/95        | 900        | 21                  | 0.63 |
| $^{13}$CO  | $J=1–0$      | 07/97      | 110                  | 200                  | 21                  | 0.74 |
|            | $J=2–1$      | 09/93      | 220                  | 660                  | 21                  | 0.63 |
| CI         | $^3P_1–^3P_0$ | 11/96      | 492                  | 1900                 | 10                  | 0.53 |

1 The James Clerk Maxwell Telescope is operated on a joint basis between the United Kingdom Particle Physics and Astrophysics Council (PPARC), the Netherlands Organisation for Scientific Research (NWO) and the National Research Council of Canada (NRC).
Fig. 1. Spectra observed towards positions A, B and C in NGC 7331 (see Sect. 2). Top row: $J=1-0$ CO; second row: $J=2-1$ CO; third row: $J=3-2$ CO; bottom row: [CI]. Horizontal scale is LSR velocity in km s$^{-1}$, vertical scale is $T_A^*$ in K. To convert to $T_{mb}$, multiply $T_A^*$ by 1.35 ($J=1-0$ CO), 1.45 ($J=2-1$ CO), 1.72 ($J=3-2$ CO) and 1.89 ([CI]), respectively.

Note: CO is marked by solid lines, $^{13}$CO multiplied by three is marked by dashed lines.
3.1. CO distribution

In the $J=1-0$ and $J=2-1$ transitions, the integrated intensities of both CO isotopes are rather similar for positions A and B, indicating a fairly smooth central distribution of relatively strong CO. This is consistent with the large (50%) fraction of flux found to be missing by Tosaki & Shibayama (1997) in their $J=1-0$ interferometer map. The results presented here and by von Linden et al. (1996) are, however, inconsistent with the folded major axis profile obtained by Young & Scoville (1982) and shown in more detail by Young et al. (1995), which exhibits both a pronounced lack of CO at the centre and a strong peak at a radial distance of 45$''$ (3 kpc). From the data in Table 2 and the results obtained by von Linden et al. (1996), it appears that the central integrated value given by Young et al. (1995) is too low by more than a factor of two. Thus, there is no significant central 'hole' in the distribution of CO emission, at least not on the scale of our 20$''$ beam.

A full-resolution contour map of the $J=2-1$ CO intensity, integrated over the velocity range of 530 to 1130 km s$^{-1}$ is shown in Fig. 2. The map shows a good overall resemblance to the $J=1-0$ CO map obtained at slightly lower resolution by von Linden et al. (1996). This is also true for the major axis position-velocity diagram (not shown here). In Fig. 2, the elliptical outline of a low-contrast ring around the center can be discerned; peaks of CO emission occur at positions 30$''$ north and 50$''$ south. The latter two more or less correspond to the radial distance of the molecular ring proposed by Young & Scoville (1982). The map covers the brightest part of the optical image also shown in Figure 2 (for better images, see panel 40 in the atlas by Sandage & Bedke 1988). In this image, a large, overexposed bulge is surrounded by dust lanes and irregular spiral arms traced by HII regions. The reddening of NGC 7331 occurs in this western spiral arm to the bulge, especially on the western side. Most of the reddening of NGC 7331 occurs in this western spiral arm (Telesco et al. 1982; Bianchi et al. 1998). On the eastern side of the CO map, faint emission due to a more distant

### Table 3. CO and CI line intensities in NGC 7331

| Transition | Resolution ($''$) | $T_{mb}$ (mK) | $\int T_{mb}dV$ (K km s$^{-1}$) |
|------------|------------------|---------------|-------------------------------|
| $J=1-0$   |                  |               |                               |
| $^{12}$CO  | 21               | 162           | 26$\pm$2                     |
| $^{13}$CO  | 21               | 21            | 3.9$\pm$0.4                  |
| $J=2-1$   |                  |               |                               |
| $^{12}$CO  | 21               | 100           | 14$\pm$2                     |
| $^{13}$CO  | 21               | 13            | 2.5$\pm$0.6                  |
| $J=3-2$   |                  |               |                               |
| $^{12}$CO  | 14               | 43            | 7.5$\pm$1.3                  |
| $^{13}$CO  | 21               | 49            | 8.8$\pm$1.5                  |
| $^{3}P_{1-3}P_{0}$ CI | 10            | 30            | 1.9$\pm$0.3                  |

**Notes to Table 3:**

a. From Young et al. (1995); b. From Elfhag et al. (1996); c. Extrapolated value; d. From von Linden et al. (1996)
major spiral arm is seen as well. The HI map obtained by Begeman (1987) at a very similar resolution shows an incomplete ‘ring’ of neutral hydrogen. The CO emission from the outlying spiral arm coincides with a relatively bright part of this HI ‘ring’. Most of the CO emission is, however, well inside it and coincides with the radio continuum ring mapped by Cowan et al. (1994). The main CO peaks are at the northern and southern extremities of the radio continuum ring.

In the velocity-integrated single-dish CO map (Fig. 2), the ring is only weakly visible. Its presence is more clearly revealed in the interferometer map of Tosaki & Shioya (1997) and in Fig. 3. This figure shows the distribution over velocity bins of 40 km s$^{-1}$ of (1997) and in Fig. 3. This figure shows the distribution over velocity bins of 40 km s$^{-1}$ only. Between velocities $V_{\text{LSR}} = 600$ and 1000 km s$^{-1}$, the maps show a double structure. The double-peak structure seen in Fig. 3 extends over most of the part of NGC 7331 characterized by rigid rotation (cf. von Linden et al. 1996). A similar pattern, with the limitations imposed by interferometric techniques, is also evident in the channel maps published by Tosaki & Shioya (1997).

### 3.2. Line ratios

The $^{12}$CO/$^{13}$CO isotopical ratios of 6 – 7 are somewhat low compared to typical values around 10 found in most other external galaxies, but given the low IRAS $f_{60}/f_{100}$ ratio of 0.3 (Rice et al. 1988) this is in line with the results obtained by Aalto et al. (1991). We find a $^{12}$CO $J=2–1/^{13}$CO over the same region, but now integrated over velocity bins of 40 km s$^{-1}$ only. Between velocities $V_{\text{LSR}} = 600$ and 1000 km s$^{-1}$, the maps show a double structure. The double-peak structure seen in Fig. 3 extends over most of the part of NGC 7331 characterized by rigid rotation (cf. von Linden et al. 1996). A similar pattern, with the limitations imposed by interferometric techniques, is also evident in the channel maps published by Tosaki & Shioya (1997).

In the velocity-integrated single-dish CO map (Fig. 2), the ring is only weakly visible. Its presence is more clearly revealed in the interferometer map of Tosaki & Shioya (1997) and in Fig. 3. This figure shows the distribution over velocity bins of 40 km s$^{-1}$ only. Between velocities $V_{\text{LSR}} = 600$ and 1000 km s$^{-1}$, the maps show a double structure. The double-peak structure seen in Fig. 3 extends over most of the part of NGC 7331 characterized by rigid rotation (cf. von Linden et al. 1996). A similar pattern, with the limitations imposed by interferometric techniques, is also evident in the channel maps published by Tosaki & Shioya (1997).

### 4. Analysis and discussion

#### 4.1. Modelling of observed line intensities

We have modelled the observed intensities and their ratios by assuming the presence of two molecular gas components of different temperature and density, a relatively cold component dominating the $J=1–0$ emission and a warmer component becoming progressively more important in the higher transitions. We have used the radiative transfer models from the Leiden astrochemistry group (Jansen 1995; Jansen et al. 1994); we included a background radiation field of $T_{\text{bg}} = 2.73$ K. In these models kinetic temperature, molecular hydrogen density and CO respectively C column densities function as input parameters. A further constraint is provided by the chemical models discussed by Van Dishoeck & Black (1988) which show a strong dependence of the $N(C)/N(CO)$ column density ratio around molecular hydrogen column densities of about $10^{21}$ cm$^{-2}$. Above $N(H_2) = 2 \times 10^{21}$, virtually all carbon is in CO, whereas below $N(H_2) = 2 \times 10^{20}$ cm$^{-2}$ virtually all carbon is in C. The CI and CO intensities observed in position A, together with the sensitivity of the C/CO ratio to H$_2$ column density provide rather stringent constraints on the models acceptable for at least the center of NGC 7331.

Although the available data do not allow a precise and unique determination of the physical condition of the molecular gas in NGC 7331, they serve well to constrain the parameter space of possible solutions. For instance, cold component CO column densities cannot exceed $N(CO) \approx 10^{17}$ cm$^{-2}$ and warm component kinetic temperatures cannot be lower than 20 K without conflicting with observed $^{12}$CO and $^{13}$CO ratios. In Table 5 we list a few representative models. Note that the CO column densities listed in Table 5 are those of a single model cloud. We assume a homogeneous population of such model clouds, non-shadowing in position-velocity space, so that the actual galaxy beam-averaged column density is the sum of the model cloud column densities in the beam multiplied by their beam filling factor.

In models 4 through 7 we vary the cold component input parameters, and assume a warm component of 30 K and density $n(H_2) = 1000$ cm$^{-3}$. In models 2 and 3, we have changed the warm component temperature to 40 K and 20 K, and in model 1 we assume a more complex situation. In addition to the warm component, the cold component itself is structured into a high-density and a low-density contributor. It is a scaled version of the single-temperature, dual-density model ($T_{\text{kin}} = 10$ K; $n(H_2) = 100$ cm$^{-3}$ and 3000 cm$^{-3}$) applied to the M 31-D 478 complex by Israel et al. (1998). Although a warm component must be included, its nature is unclear. Given the large linear beamsize (1.5 x 5.5 kpc) in the plane of the galaxy, this warm component may represent discrete, starforming cloud complexes at some distance from the center. In all models, $J=1–0$ CO intensities are dominated by emission from the cold component with contributions of about 75%, 70% and 85% for positions A, B and C respectively. In contrast, the $J=3–2$ CO intensities are all dominated by emission from the warm component. For the optically thin $^{13}$CO transitions the
Fig. 3. $J=2-1 \ ^{12}\text{CO}$ channel maps of NGC 7331. Emission is integrated over velocity bins of 40 km s$^{-1}$; central velocities are marked in the panels. Contours are in steps of $\int T_{\text{mb}}dV = 2$ K km s$^{-1}$.

Table 4. Integrated line ratios in the centre of NGC 7331

| Transitions | pos. A  | pos. B  | pos. C  | D 478$^a$ |
|-------------|---------|---------|---------|-----------|
| $^{12}\text{CO} (2-1)/(1-0)$ | 0.54±0.10 | 0.51±0.10 | 0.35±0.11 | 0.42±0.08 |
| $^{12}\text{CO} (2-1)/(2-1)$ | 0.63±0.15 | 0.78±0.35 | 1.0±0.41 | 0.33±0.10 |
| $^{13}\text{CO} (2-1)/(1-0)$ | 0.64±0.2  | 0.55±0.1  | —       | 0.45±0.15 |
| $^{12}\text{CO}/^{13}\text{CO} (1-0)$ | 6.7±1.1   | 7.8±1.2   | —       | 8.8±1.8   |
| $^{12}\text{CO}/^{13}\text{CO} (2-1)$ | 5.6±1.6   | 7.2±1.6   | 5.8±3.3 | 8.4±1.7   |
| CI/CO(2-1) | 0.21±0.07 | —        | —       | 0.24±0.05 |

Note: $^a$ Dark cloud in M 31; see Allen et al. (1995); Loinard & Allen (1998); Israel et al. (1998).

Table 5. Model parameters for NGC 7331

| Model | Kinetic Gas | Cold Component | Warm Component |
|-------|-------------|----------------|----------------|
|       | $T_{\text{kin}}$ | $n(\text{H}_2)$ | $N(\text{CO})/dV$ | $T_{\text{kin}}$ | $n(\text{H}_2)$ |
|       | (K)         | (cm$^{-3}$)    | (10$^{17}$ cm$^{-2}$ K km s$^{-1}$)$^{-1}$ | (K)         | (cm$^{-3}$) |
| 1     | 10/10$^a$   | 100/3000       | 0.7/7.0        | 30          | 3000         |
| 2     | 10          | 300            | 1.0            | 40          | 1000         |
| 3     | 10          | 300            | 1.0            | 30          | 1000         |
| 4     | 10          | 300            | 1.0            | 20          | 1000         |
| 5     | 10          | 100            | 1.0            | 30          | 1000         |
| 6     | 10          | 300            | 0.1            | 30          | 1000         |
| 7     | 10          | 100            | 0.1            | 30          | 1000         |

Note: $^a$ Cold component assumed to consist of both low and high density gas as in D 478; see Israel et al. (1998).
situation is less clearcut: if we assume an intrinsic isotopic ratio of 100, emission from the cold component contributes about 25% to the $J=1–0$ emission from positions A and B, whereas this fraction increases to about 45% if we assume an isotopic ratio of 50.

### 4.2. CO and C column densities

In order to relate neutral carbon and carbon monoxide column densities to that of molecular hydrogen, we have used $[\text{C}]/[\text{H}]$ gas-phase abundance ratios estimated from the $[\text{O}]/[\text{H}]$ abundance. From the data tabulated by Zaritsky et al. (1994) we determined for the central beam (position A) $12 + \log (\text{O}/\text{H}) = 9.2$, i.e. $[\text{O}]/[\text{H}] = 1.5 \times 10^{-3}$. Although high, such an oxygen abundance is normal for galaxy centers (Garnett et al. 1997; van Zee et al. 1998). Using results given by Garnett et al. (1999), notably their Figures 4 and 6, we arrive at an estimated carbon abundance $[\text{C}]/[\text{H}] = 2 \pm 1 \times 10^{-3}$. As a significant fraction of all carbon will be tied up in dust particles, and not be available in the gas-phase, we adopt a fractional correction factor $\delta_c = 0.33$. Neglecting contributions by e.g. $^{13}\text{CO}$ and ionized carbon, we thus find $N_{\text{H}} = [2N(\text{H}_2) + N(\text{HI})] \approx 1700 [N(\text{CO}) + N(C)]$ with a factor of two uncertainty in the numerical factor. Similarly, we find for the off-center positions B and C numerical factors of 2300 and 3000. The beam-averaged column densities in Table 6 have been obtained by scaling the model cloud column densities by the ratio of actual observed CO intensity to predicted model CO intensity.

The results of our model calculations are given in Table 6. In the table we give the predicted $[\text{CI}]$ intensity $I_{\text{CI}}$, which can be verified observationally, the calculated beam-averaged column densities for both CO and C, the $\text{H}_2$ column densities derived from these using the $N_{\text{H}}/N_C$ ratios and $N(\text{HI})$ values given, as well as the implied CO to $\text{H}_2$ conversion factor $X = N(\text{H}_2)/I_{\text{CO}}$. The neutral carbon intensities $I(\text{CI})$ were calculated under the assumption that a significant fraction (0.6–0.7) of the total atomic carbon column density is ionized and present in the form of $[\text{CII}]$. Changes in the input CO column densities do not strongly affect the resultant C column density: a substantially higher $N(\text{CO})$, for instance, implies a lower $N(C)/N(\text{CO})$ ratio, yielding a relatively unchanged $N(C)$. We have also performed the calculations for a ratio of 50. Generally, the ratio of 100 provides a better fit to the $^{13}\text{CO}$ data than the ratio of 50. As the end results for the two sets are moreover very similar, we have not included the latter in the table. The results of all models are given for position A, where we have also measured the $[\text{CI}]$ intensity in a $10''$ beam. However, the models apply to measurements in the $21''$ beam observed or synthesized for CO. If atomic carbon is at a minimum in the center, $[\text{CI}]$ intensities in a twice larger beam may be somewhat higher, perhaps by as much as 40%. Table 6 shows that model 1 yields a very good fit, whereas models 2 through 5 are marginally possible and models 6 and 7 are ruled out. Model 1 is not unique; various other combinations of somewhat different kinetic temperatures for both cold and warm gas and somewhat different densities, yield very similar results.

As models 6 and 7 are ruled out for position A and models 2 through 5 yield almost identical final results, we present only models 1 and 3 for positions B and C. The results for position C have relatively large uncertainties due to the weakness of its emission, and the lack of a $J=1–0$

| Model | Predicted CI Intensity $\int T_{\text{mb}}dV$ (K km s$^{-1}$) | Beam-Averaged Column Densities $N(\text{CO})$ (10$^{20}$ cm$^{-2}$) | Conversion Factor $X$ | Mass per Beam $M(\text{H}_2)$ ($10^7 M_\odot$) | Face-on Mass Density $\sigma(\text{H}_2)$ ($M_\odot$ pc$^{-2}$) |
|-------|-----------------------------------------------|-----------------|-----------------|--------------|----------------|
|      | $N(\text{C})$ (10$^{20}$ cm$^{-2}$) | $N(\text{H}_2)$ (10$^{20}$ cm$^{-2}$ K km s$^{-1}$) |                  |              |               |
|      | $M_\odot$ pc$^{-2}$ | $M_\odot$ pc$^{-2}$ |
| Position A; $N_H/N_C = 1700$; $N(\text{HI}) = 5 \times 10^{20}$ cm$^{-2}$ | | | | | |
| 1 | 2 | 0.011 | 0.006 | 12 | 0.4 | 3 | 5 | 5 | 8 |
| 2 | 4 | 0.012 | 0.040 | 42 | 1.5 | 11 | 15 | 17 | 24 |
| 3 | 4 | 0.009 | 0.041 | 40 | 1.5 | 10 | 14 | 16 | 23 |
| 4 | 4 | 0.008 | 0.042 | 40 | 1.5 | 10 | 14 | 16 | 23 |
| 5 | 4 | 0.009 | 0.051 | 48 | 1.9 | 13 | 18 | 20 | 28 |
| 6 | 8 | 0.005 | 0.045 | 39 | 1.5 | 10 | 15 | 16 | 23 |
| 7 | 9 | 0.008 | 0.089 | 80 | 3.1 | 21 | 29 | 33 | 46 |
| Position B; $N_H/N_C = 2300$; $N(\text{HI}) = 9 \times 10^{20}$ cm$^{-2}$ | | | | | | |
| 1 | 2.5 | 0.011 | 0.007 | 16 | 0.6 | 4 | 7 | 7 | 12 |
| 3 | 4 | 0.006 | 0.030 | 37 | 1.5 | 10 | 15 | 15 | 23 |
| Position C; $N_H/N_C = 3000$; $N(\text{HI}) = 9 \times 10^{20}$ cm$^{-2}$ | | | | | | |
| 1 | 0.7 | 0.004 | 0.003 | 8 | 0.8 | 2 | 4 | 3 | 7 |
| 3 | 1.3 | 0.002 | 0.013 | 19 | 1.9 | 5 | 8 | 8 | 13 |
13CO measurement. The results are not greatly different from those obtained at position A. Column densities decrease, and X factors increase somewhat with radius. At $T_{\text{kin}} = 10$ K, the $^{3}\text{P}_2-^{3}\text{P}_1$ [Cl] transition at 809 GHz has negligible intensity, but this becomes comparable to the $^{3}\text{P}_1-^{3}\text{P}_0$ 492 GHz transition at $T_{\text{kin}} = 30$ K. The presence of the warm component can therefore be verified by future observations of the 809 GHz [Cl] transition, for which we predict an intensity of 15–30% of the 492 GHz intensity. For the [CII] emission we expect intensities of the order of $5 \times 10^{-6}$ erg s$^{-1}$ cm$^{-2}$ sr$^{-1}$.

Beam-averaged neutral carbon to carbon monoxide column density ratios are $N(C)/N(\text{CO}) = 0.65 \pm 0.1$ and $N(C)/N(\text{CO}) = 5.5 \pm 1.0$ for models 1 and 3 respectively. The former is close to the typical values 0.2–0.5 found for the Milky Way, which can also be compared to the relationship between $X$ and metallicity found by Israel (1997).

4.3. Molecular hydrogen and the $I(\text{CO})$ to $N(\text{H}_2)$ ratio

Although any explanation of the observed CO intensities requires the presence of both cold and smaller amounts of warm molecular gas in NGC 7331, the range of admissible parameters is not fully constrained. The [Cl] intensity observed towards the center of the galaxy, however, strongly suggests a complex physical environment of the sort represented by model 1. This model is characterized by cold molecular gas (typical temperature $T_{\text{kin}} = 10$ K) present at both high and low volume densities (typically of order a few hundred and a few thousand per cc respectively), in addition to a warmer component (temperature $T_{\text{kin}} \gtrsim 20$K) of high density. This is probably a simplification: in reality a range of densities and temperatures is likely to be present. As the large linear beamsize (1.5 kpc along the major axis, 0.5 kpc along the minor axis) only provides results averaged over a large radial range, the spatial distributions of the cold and the warm gas within the beam may well be different. Both kinetic temperature and mean molecular gas density in the centre of NGC 7331 are typically an order of magnitude below the values found in later-type starburst galaxies such as NGC 253 and M 82 (Israel et al. 1995; Wall et al. 1991).

Our models suggest that a large fraction of the CO emission originates from cold gas of low column density. A smaller fraction originates in much denser gas, partly at higher temperatures. The cold gas in the center of NGC 7331 appears to be similar to that in cloud complexes such as D 478 in M 31 dark and the Taurus-Auriga complex in the Milky Way; most likely, it is highly fragmented and filamentary (Israel et al. 1998). The warm gas may be heated by the nucleus and by luminous stars in the inner spiral arms and the ‘molecular ring’. The presence of energetic photons in the inner part of NGC 7331 is betrayed by Hα+[NII] emission (see Fig. 5 by Smith & Harvey 1996) and more directly by significant UV emission (Wesselius et al. 1982) unlikely to be dominated by the spiral arms because of their high dust content (Bianchi et al. 1998).

The evaluation of the models in Tables 5 and 6 assumes a radiation field $I_{\text{UV}} \approx 1$, corresponding to $I_{1000} = 4.5 \times 10^{-8}$ photons s$^{-1}$ cm$^{-2}$ which is consistent with the longer-wavelength UV data by Wesselius et al. (1982). Such a low radiation field density is also indicated by the strength of the 7.7 and 11.3 µm dust emission features (Smith 1998). The beam-averaged column densities in Table 6 are relatively insensitive to changes in the assumed $I_{\text{UV}}$, because in the cold diffuse gas, most carbon is already in C rather than in CO, whereas the much smaller filling factor of the dense gas greatly reduces the effect of changes in the $N(C)/N(\text{CO})$ ratio on the beam-averaged neutral carbon column density. Moreover, we expect only limited variation (by a factor of 2–3) in the radiation field density over at least the inner 5 kpc because of the smooth distribution of Hα emission as well as the far-infrared emission between 50µm and 200µm (Smith & Harvey 1996; Alton et al. 1998). The quiescence of the spiral arms is illustrated by the strong excess of 450 and 850µm emission from cold dust (Bianchi et al. 1998). Thus, the spiral arms contain a relatively large amount of cold dust especially in comparison with the central region. We are therefore confident of the derived $N(\text{H}_2)$ values in Table 6.

As C and O abundances in NGC 7331 are 2–5 times higher than those in the Solar Neighbourhood, and radiation fields are not particularly intense, we expect CO in NGC 7331 to be relatively well-shielded, so that the CO to H2 conversion factor X should be lower than that in the Solar Neighbourhood, i.e. fewer H2 molecules per unit CO intensity. Indeed we find values of $X$ lower than the value of $2 \times 10^{20}$ cm$^{-2}$/K kms$^{-1}$ assumed for the Milky Way, which can also be compared to the relationship between $X$, radiation field intensity and metallicity found by Israel (1997). For positions A, B and C we take $[\text{O}]/[\text{H}]$ abundance ratios of 1.5, 1.3 and 1.1 in units of $10^{-3}$ respectively (Zaritzky et al. 1994). From high-resolution far-infrared surface brightnesses (Smith & Harvey 1996), HI column densities (Begeman 1987) and eqn. (3b) from Israel (1997), we predict values $X = 0.8$, 0.7 and 1.0 in units of $10^{20}$ cm$^{-2}$/[(K kms$^{-1}$)$^{-1}$] for positions A, B and C respectively. These are very close to the results from the preferred model 1, and a factor of two or more below the results for the other models. Neglect of the radiation field term in Israel’s (1997) eqn. (3b), i.e. use of his eqn. (4) predicts in the same units $X = 0.15$, 0.25 and 0.4 for positions A, B and C, i.e. much lower than any of the model results. We conclude that the low values of $X$ in the preferred model 1 are in good agreement with both the high abundances in NGC 7331 and the relationship between $X$, radiation field intensity and metallicity found by Israel (1997).
With respect to the value of $X$ derived for position A it should be noted that the large linear beamsize includes both the center of NGC 7331 and more outlying regions along the minor axis. If the latter were to be characterized by an $X$ value closer to that of position B, the actual central $X$ value would be significantly lower. For instance, if we assign $X = 0.6 \times 10^{20} \text{cm}^{-2}/\text{K kms}^{-1}$ to the outer half of the CO emission, the inner half would have $X = 0.2 \times 10^{20} \text{cm}^{-2}/\text{K kms}^{-1}$, an order of magnitude less than the Milky Way value, and well below what is suggested by the high metallicity. Such a very low value would, however, not be unexpected. For the Milky Way centre, Sodroski et al. (1995) conclude to an $X$-factor 3 – 10 times smaller than the ‘standard’ Galactic value. The COBE Galactic Centre data presented by Bennett et al. (1994) imply lower CO transition ratios somewhat similar to those in NGC 7331.

Another way of verifying the derived $H_2$ column densities is provided by the submillimeter observations presented by Bianchi et al. (1998). For $F_{250\mu m} = 50$ mJy and $T = 20 \pm 3 \text{K}$ in a $30'' \times 40''$ beam (Bianchi et al. 1998), we derive a beam-averaged $A_V = 6.6$ (-1.2, +2.2). Furthermore assuming that the dust to gas ratio is proportional to metallicity, we modify the Galactic relation between total hydrogen column density and visual extinction (Bohlin et al. 1978) to $N_{H} = 0.6 \times 10^{21} A_V \text{cm}^{-2}$. This implies a column density $N(H_2) = 2(-0.4,+0.6) \times 10^{21} \text{cm}^{-2}$ (corresponding to $X = 0.75(-0.15,+0.25) \times 10^{20}$). The similarly obtained result for position B is slightly lower. These results are thus in rather good agreement, given the various uncertainties, with $N(H_2) = 1.2 - 1.6 \times 10^{21} \text{cm}^{-2}$ and $X = 0.4 - 0.6 \times 10^{20}$ found for positions A and B using model 1.

Comparison of the models and the observations allows us to draw some general conclusions on the distribution of molecular hydrogen in NGC 7331. In model 1, relative amounts of cold/tenuous, cold/dense and warm/dense molecular hydrogen gas are 45%, 30% and 25% for positions A and B. The results for position C seem to indicate a somewhat higher contribution by warm molecular gas. Using the beam-averaged $H_2$ column densities and the model $H_2$ volume densities, we find that the average line of sight within the beam contains cold/tenuous $H_2$ over about 2 pc (Model 1, positions A and B) to 0.7 pc (Model 1, position C). Both the cold and the warm dense component have average line-of-sight extents a factor of 50 lower. However, the observed CO temperatures are much lower than the model excitation temperatures, indicating small beam-filling factors for the molecular material. Assuming individual lines of sight within the beam to be either empty, or homogeneously filled with molecular gas, we find for those line of sights that do contain molecular gas extents of about 20 pc (cold tenous gas), 2.5 pc (cold dense gas) and 25 pc (warm dense gas); these numbers are indicative of the maximum source size that can be expected.

Application of model 3 yields somewhat different results. Here, most of the molecular gas is in the cold/tenuous form rather than in the warm/dense phase: only 17% warm gas is required at position A, and about 5% at positions B and C. Average line of sight extents are 3.5 pc for cold gas at positions A and B, and half that at position C. After correction for beam filling, we find lines of sight extents of typically 115 pc for the cold molecular gas and 15% or less of that for warm gas. Only at position C a more uncertain extent of 20 pc is obtained.

The derived line of sight extents are much smaller than the length of the line of sight traversing the galaxy, which is about four times its thickness. Although the latter is not known, this length can be estimated at well in excess of a kiloparsec. Thus, only a small fraction of the volume sampled by the beam at each of the analyzed positions is filled with molecular material. This material is highly clumped or distributed in filamentary form.

4.4. Radial distribution of molecular gas

In the case of highly-inclined ring structures, major-axis position-velocity diagrams may give a misleading impression of the actual radial distribution of emitting material, because at the tangential points substantially longer lines of sight contribute to the emission. To determine the actual distribution of CO as a function of radial distance from the centre spectra, we have fitted an inclined axisymmetric disk model to the data in the velocity-integrated map (Fig. 3) by applying the Richardson-Lucy iterative scheme (Lucy 1974). In principle, with a priori knowledge of the (CO) velocity field, this technique can also be used to obtain radial distributions with a spatial resolution higher than that of the observing beam (Scoville, Young & Lucy 1983). Fig. 4 shows the fitted radial distribution of the velocity-integrated $J=2–1$ CO emission.

The fitted profile corresponds to the face-on radial distribution of $I'(CO) = \int (T^2_\text{a}(CO) dV)$. The CO luminosity starts at $I'(CO) = 4 \text{ K km s}^{-1}$ in the center, reaches a minimum at $R \approx 1.75 \text{kpc}$, and the reaches a maximum at $R \approx 3.5 \text{kpc}$ after which it drops smoothly to $I'_\text{CO} = 2 \text{ K km s}^{-1}$. The ring-to-disk intensity contrast ratio is about 0.6. The molecular ‘ring’ is clearly discernible, but it does not dominate the CO distribution in the galaxy. Both the major-axis CO distribution and the fitted radial CO profile are different from those of M 31, where most of the CO is found farther out in the spiral arm ‘ring’ at $R=9 \text{kpc}$, and very little CO occurs at the centre (Dame et al. 1994).

In order to determine the radial distribution of interstellar gas in NGC 7331, we have converted the CO radial profile to a radial distribution of $H_2$ mass densities, using the $J=1–0/J=2–1$ CO ratios and $X$ values from Tables 4 and 6, and combined these with the radial HI profile published by Begeman (1987). Both the radial $H_2$ and HI profiles are also shown in Figure 4. In the inner 4.5
kpc, the H$_2$ mass dominates that of HI by about 40%. Beyond this, HI becomes increasingly dominant. The radial distribution of molecular gas reaches its peak (at $R = 3.1$ kpc) well before that of HI (at $R \approx 10$ kpc). Although the radial $J=2$--$1$ CO profile exhibits a relatively low contrast between the ring feature and the underlying disk emission, the radially increasing transitional ratios and X-values serve to enhance the contrast in H$_2$. The central region is not empty, but the H$_2$ mass density inside the ring is only 75% of that in the ring; due to the lack of HI in the center, the relative mass density of all hydrogen is even lower with 55% of the ring value. The face-on H$_2$ mass distribution increases from $\sigma_{{H_2}} = 6$ M$_\odot$ pc$^{-2}$ to 8 M$_\odot$ pc$^{-2}$ at $R = 3.1$ kpc. The total hydrogen radial mass-density distribution increases from a central value $\sigma_{{HI+H_2}} = 8$ M$_\odot$ pc$^{-2}$ to $\sigma_{{HI+H_2}} = 14$ M$_\odot$ pc$^{-2}$ at $R = 3.5$ kpc and then drops slowly. The gaseous face-on (including helium) of the total mass was estimated from the rotation curves given by Rubin et al. (1965) and Begeman (1987), assuming a spherical bulge and circular velocities. Inside the ring, the gas-to-total mass ratio $M_{\text{gas}}/M_{\text{dyn}}$ is about 1%. In the ring, it rises to 1.5%, and then slowly climbs to 3%. From Begeman’s (1987) data, neglecting H$_2$, we find in comparison a global ratio $M_{\text{gas}}/M_{\text{dyn}}$ of 3.2%. Even with the dominant contribution by H$_2$, the gas in the inner part of NGC 7331 is only a minute fraction of the total mass.

Finally, it is of interest to compare the radial gas distributions to the radial far-infrared profiles representing interstellar dust. The 100$\mu$m far-infrared profile (Smith & Harvey 1996) is rather flat in the center, reaching a very minor maximum at about 2 kpc, after which a steep decline sets in. The 450$\mu$m and 850$\mu$m profiles show radially increasing intensities that reach a peak at about 3 kpc, the 850$\mu$m profile peaking a little farther out than the 450$\mu$m profile (Bianchi et al. 1998). The H$_2$ mass-density peaks at $R = 3.1$ kpc, just about coincident with the 850$\mu$m maximum. At the location of the molecular ‘ring’ peak, 100$\mu$m intensities are about 80% of those in the center. However, the total gas mass-density peaks slightly farther out at $R = 3.8$ kpc. Thus, emission from warm dust peaks well inside the molecular ring, and both molecular gas and cold dust peak inside the radius of highest gas mass-density. Beyond the ring peak, the decline of the 450$\mu$m and 850$\mu$m emission more or less follows that of the H$_2$ mass density profile. We conclude that the interstellar dust is hottest in the central region, where gas mass-densities are lowest. The mean dust temperature defined by the far-infrared ratios smoothly decreases from the center reaching a shallow minimum at about $R = 3$ kpc, i.e. at the H$_2$ peak, beyond which it appears to increase slightly.

4.5. Origin of bulge molecular gas and the ring

Various mechanisms for the occurrence of ring morphologies have been suggested in the literature. Interaction between magnetic fields and the gas distribution were proposed and tested by Battaner et al. (1988). Inner Lindblad resonances may be responsible (Kormendy & Norman 1979), and a ringlike feature may also result from evacuation of gas from the central regions by stellar winds (cf. Faber & Gallagher 1976; Soifer et al. 1986, Muñoz-Tuion & Beckman 1988). Finally, as Young & Scoville (1982) suggested for NGC 7331, a ringlike appearance may also be caused by the nuclear bulge having used up the originally present molecular gas in the center.

In NGC 7331, the solid-body rotation curve rises rapidly out to $R = 3.5$ kpc after which it flattens and reaches a broad maximum at $R = 6$ kpc (see also von Linden et al. 1996). The ring is thus located just at the radius where rigid rotation is lost, but well within the radius of maximum rotational velocity ($R_{\text{ring}} = 0.6 R_{\text{Vmax}}$). This is unlike M 31, where the molecular ring is found at a radius twice that of peak rotational velocity (Brinks & Burton 1984; Dame et al. 1993). Both the molecular ring and the boundary of the solid-body rotation region are also just at the radius at which the light of the disk becomes dominant over that of the bulge (cf. Begeman 1987). Although the radius of the mostly nonthermal radio continuum ring radius is more difficult to determine because of its inhom-
5. Conclusions

1. Analysis of the $J=2–1 \ ^{12}\text{CO}$ distribution and kinematics shows the presence of enhanced molecular emission in a ringlike zone in NGC 7331, peaking at a radial distance of 3.5 kpc with a width of about 2 kpc. At $R = 3.5$ kpc, the velocity-integrated CO intensity of the ring itself is about 0.6 times that of the underlying more smoothly distributed CO emission that fills the entire bulge of NGC 7331.

2. The velocity-integrated CO intensities in the center of NGC 7331 decrease strongly with increasing rotational level. The intensities in the $J=1–0$, $J=2–1$, $J=3–2$ transitions are in the ratio of 1.0 : 0.55 : 0.35 respectively. The observed $^{12}\text{CO}/^{13}\text{CO}$ isotopic ratios are 6.7 and 5.6 in the $J=1–0$ and $J=2–1$ transitions respectively. Positions at larger radial distances have similar ratios, albeit with somewhat stronger $J=3–2$ CO emission, and weaker $^{13}\text{CO}$ emission. Weak [CI] emission was detected from the center.

3. Modelling of the observed line ratios suggest a multi-component molecular medium. Gas with a kinetic temperature of about 10 K appears to be present at both low and high densities. At high densities, a warmer component with a kinetic temperature of 20 K or more is also present within the observing beams. The gas is probably distributed in a clumpy and filamentary form.

4. Assuming a $[\text{C}] / [\text{H}]$ abundance ratio of the order of $1–2 \times 10^{-3}$, the mean CO-to-H$_2$ conversion factor is $X_{\text{N7331}} = 4 \times 10^{19}$ cm$^{-2}$ in the bulge region, and double that value in the ring and beyond. These values are well below those found in the Solar Neighbourhood, but they are consistent with the high metallicity of NGC 7331 and with submillimeter dust observations.

5. In the bulge, interstellar gas (HI + H$_2$ + He) mass densities, projected onto the plane of the galaxy, are of the order of $11 \ M_\odot$ cm$^{-2}$. In the ring itself, now properly placed at $R = 3.1$ kpc, the gas mass density is almost twice as high. Within the ring, the interstellar gas mass is dominated by the molecular hydrogen contribution. Gas to total (dynamical) mass ratios are about 1% in the center and about 1.5% in the ring.

6. The molecular ring coincides more or less with the mostly nonthermal radio continuum ring and the 850 $\mu$m ring representing emission from cold dust. Emission from warmer dust in the 100$\mu$m wavelength range peaks well inside the molecular ring; dust temperatures appear to be decreasing with radius reaching a minimum in the ring. The radial distribution of HI reaches it maximum well beyond the molecular ring.

7. The molecular ring is well inside the radius of peak rotational velocity. Its maximum is just at the edge of the region of solid-body rotation, and just at the radius where disk light becomes dominant over bulge light. The ring is not associated with an inner Lind-
blad resonance. The molecular gas inside the ring may have originated from mass loss by late type stars in the bulge. If this is the case, the ring is probably the result of wind-driven gas removal from the center.

Acknowledgements. We are indebted to Ewine van Dishoeck and David Jansen for providing us with their detailed radiative transfer models. We also thank the JCMT personnel, in particular Remo Tilanus, for their support and help in obtaining the observations discussed in this paper, and Jeroen Stil for considerable help in producing Figure 2. The IRAM observations were kindly obtained for us by Gabriel Paubert in service mode.

References

Aalto S., Black J.H., Johansson L.E.B., Booth R.S., 1991, A&A 249, 323
Allen R.J., Lequeux J., 1993, ApJL 410, L15
Allen R.J., Le Bourlot J., Lequeux J., Pineau des Forêts G., Roueff E., 1995, ApJ 444, 157
Alton P.B., Trewhella M., Davies, J.I. et al., 1998, A&A 335, 807
Arp H.C., Kormendy J., 1972, ApJL 178, L101
Battaner E., Florido E., Sanchez-Saavedra M.L., 1988, ApJ 331, 116
Begeman K., 1987, Ph.D. Thesis, University of Groningen (NL)
Bennett C.L., Fixsen D.J., Hinshaw G., et al., 1994, ApJ 434, 587
Bianchi S., Alton P.B., Davies J.I., Trewhella M. 1998, MNRA S 298, L49
Bohlin R.C., Savage B.D., Drake J.F., 1978, ApJ 224, 132
Bosma A.: 1978, Ph.D. thesis, University of Groningen (NL)
Bottema R.: 1999, A&A 348, 77
Braine, J., Combes F., Casoli F., et al., 1993, ApJS 97, 887
Brinks E., Burton W.B., 1984, A&A 141, 195
Cowan J.J., Romanishin W., Branch D., 1994, ApJL 436, L139
Dame T.M., Koper E., Israel F.P., Thaddeus P., 1994, ApJ 418, 730
Dressel L.L., Condon J.J. 1976, ApJS 31, 187
Elfhag T., Booth R.S., Högbund B., Johansson L.E.B., Sandquist Aa., 1996, A&AS 115, 439
Fabrer S.M., Gallagher J.S., 1976, ApJ 204, 365
Garnett D.R., Shields G.A., Skillman E.D., Sagan S.P., Dufour R.J., 1997, ApJ 489, 63
Garnett D.R., Shields G.A., Peimbert M., et al. 1999 ApJ 513, 168
Israel F.P., 1997, A&A 328, 471
Israel F.P., White G.J., Baas F., 1995, A&A 302, 343
Israel F.P., van der Werf P.P., 1996, in: Cold Gas at High Redshift, ed. M.N. Bremer, P.P. van der Werf, H.J.A. Röttgering, C.L. Carilli (Dordrecht: Kluwer), p. 429
Israel F.P., Tilanus R.P.J., Baas F., 1998, A&A 339, 398
Jansen D.J., 1995, Ph.D. thesis, University of Leiden (NL)
Jansen D.J., van Dishoeck E.F., Black J.H., 1994, A&A , 282, 605
Koper E. 1993, Ph.D. thesis, University of Leiden (NL)
Kormendy J., Norman C.A., 1979, ApJ 233, 539
Lang K.R., 1992, Astrophysical Data, (New York: Springer), p. 703
Loinard L., Allen R.J., Lequeux J., 1995, A&A 301, 68
Loinard L., Allen R.J., 1998, ApJL 499, 277
Lucy L.B., 1974, ApJ 79, 745
Mediavilla E., Arribas S., García-Lorenzo B., del Burgo C., 1997, ApJ 488, 682
Muñoz-Tuñon C., Beckman J.E., 1988, Ap&SS, 147, 173
Petitpas G.R., Wilson C.D., 1998, ApJ 503, 219
Prada F., Gutiérrez C.M., Peletier R.F., McKeith C.D., 1996, ApJL 463, L9
Rubin V.C., Burbidge E.M., Burbidge G.R., Crampin D.J., 1965, ApJ 141, 759
Sandage A., Tammann G.A., 1987, A Revised Sneyaple-Ames Catalog of Bright Galaxies, second edition, Carnegie Institution of Washington Publication 635 (Washington, D.C.: Carnegie Institution of Washington).
Sandage A., Bedke J., 1988, Atlas of Galaxies, NASA-SP 496 (Washington, D.C.: NASA).
Scoville N.Z., Solomon P.M., 1975, ApJ 199, L105
Scoville N.Z., Young J.S., Lucy L.B., 1983, ApJ 270, 443
Smith B.J., 1998, ApJ 500, 181
Smith B.J., Harvey P.M., 1996, ApJ 468, 139
Sodroski T.J., Odegard N., Dwek E., et al., 1995, ApJ 452, 262
Soifer B.T., Rice W.L., Mould J.R., et al., 1986, ApJ 304, 651
Stark A.A. 1979, Ph.D. thesis, Princeton University (USA)
Stockdale C.J., Romanishin W., Cowan J.J., 1998 ApJ 508, 33
Stutzki J., Graf U.U., Honingh C.E., et al., 1997, ApJL 477, 33
Telesco C.M., Gatley I., Steward J.M., 1982, ApJ 263, L13
Tosaki T., Shioya Y., 1997, ApJ 484, 664
Tully R.B., 1988, Nearby Galaxies Catalog. (Cambridge: Cambridge University Press)
van Dishoeck E.F., Black J.H., 1988, ApJ 334, 771
van Zee L., Salzer J.J., Haynes M.P., O’Donoghue A.A., Balonek T.J., 1998 AJ 116, 280
von Linden S., Reuter H.-P, Heidt J., Wielebinski R., Pohl M., 1996, A&A 315, 52
Wall W.F., Jaffe D.T., Israel F.P., Bash F.N., 1991, ApJ 380, 384
Wesselius P.R., van Duinen R.J., de Jonge A.W., et al., 1982, A&AS 49, 427
White G.J., Ellison B., Claude W.R.F., Matheson D.N., 1994, A&A 284, L23
Young J.S., Scoville, N.Z., 1982, ApJL 260, L41
Young J.S., Xie S., Tacconi L., et al. 1995, ApJS 98, 219
Zaritsky D., Kennicutt R.C., Huchra J.P., 1994, ApJ 420, 87