Theory of a Magnetically-Controlled Quantum-Dot Spin Transistor

Daniel Urban, Matthias Braun, and Jürgen König
Institut für Theoretische Physik III, Ruhr-Universität Bochum, 44780 Bochum, Germany
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We examine transport through a quantum dot coupled to three ferromagnetic leads in the regime of weak tunnel coupling. A finite source-drain voltage generates a nonequilibrium spin on the otherwise non-magnetic quantum dot. This spin accumulation leads to magnetoresistance. A ferromagnetic but current-free base electrode influences the quantum-dot spin via incoherent spin-flip processes and coherent spin precession. As the dot spin determines the conductance of the device, this allows for a purely magnetic transistor-like operation. We analyze the effect of both types of processes on the electric current in different geometries.

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I. INTRODUCTION

Electric transport properties depend on magnetic system degrees of freedom as demonstrated by e.g. the giant-magneto-resistance (GMR) and tunnel-magneto-resistance (TMR) effects. In these it is used that charge currents can be tuned by changing the relative orientation of magnetic moments in magnetic heterostructures. For example, the transmission through an interface between two ferromagnetic electrodes decreases as the relative angle between the electrodes' magnetization directions increases, which is known as the spin valve effect.

If a non-magnetic spacer region is inserted between source and drain, the information about the relative spin orientation is mediated between source and drain by spin accumulation in the intermediate region. Scattering at the interfaces may also contribute significantly to transport. Manipulation of the accumulated spin opens the possibility to modify the source-drain current. Such manipulation was suggested to be achievable electrically with the help of spin-orbit coupling as proposed by Datta and Das. It may also be accomplished magnetically, e.g. by external magnetic fields or by additional leads. In addition, in low-dimensional systems the significant charging energy also affects transport, giving rise to the well-known Coulomb staircase, but also affecting the spin-dependence of transport.

In this paper we study a magnetically-controlled quantum-dot spin transistor, in which the transport behavior is affected by the interplay of spin accumulation and Coulomb charging. We consider a single-level quantum dot with strong Coulomb interaction that is connected to three ferromagnetic leads. The base lead which is kept charge-current free, so that the source-drain current is magnetically affected by the base lead only via manipulation of the accumulated dot spin.

There are two qualitatively different ways in which the current-free base lead affects the quantum-dot spin. One is that the base electrode offers a channel of spin relaxation. An electron with, say, spin up tunnels out of the dot and an electron with spin down tunnels in. Such spin-flip processes, which are accompanied by a spin but no charge current in the base electrode, reduce the spin accumulation on the dot. The strength of this relaxation depends on the orientation of the base electrode's magnetization direction relative to the spin accumulation. This scheme has been proposed to realize a "spin-flip transistor" with metallic islands in the absence of Coulomb interaction. In quantum dots, however, there will also be a second contribution, related to spin precession due to the exchange interaction between the quantum-dot level and ferromagnetic base electrode. In general, both types of processes play a role. The main objective of this paper is to identify and discuss the effect of both of them on the transport characteristics.

In the following Sec. we define the model Hamiltonian and the kinetic equations for the quantum dot's degrees of freedom, and derive the conductance of the spin transistor, which is discussed in Sec. In Sec. we discuss the special situation when the three magnetizations of the leads are chosen pairwise orthogonal. In this case, the spin-related resistance change is dominated by the exchange effect. We close with a summary in Sec. 

FIG. 1: The spin transistor consists of a quantum dot connected to source and drain lead by tunnel contacts. Source and drain have antiparallel magnetizations so that a nonequilibrium spin is accumulated on the dot, which modifies the conductance of the device. A floating base lead can be used to influence the dot state solely by spin currents, i.e., the source-drain conductance can be modified by the alignment of the magnetization alone.
II. MODEL HAMILTONIAN, KINETIC EQUATIONS, AND CURRENT

We study a single-level quantum dot with contacts to three ferromagnetic leads \([\text{source}(\text{left}),\ \text{drain}(\text{right}),\ \text{base}(\text{middle})]\) by tunnel junctions, described by the Hamiltonian

\[
H = H_{\text{dot}} + H_L + H_M + H_R + H_T. \tag{1}
\]

The first part \(H_{\text{dot}} = \sum_{s} \varepsilon^d c_s^\dagger c_s + U n_{1\uparrow} n_{1\downarrow}\) models the quantum dot as an Anderson impurity with a spin-degenerate electronic level \(\varepsilon\) and charging energy \(U\) for double occupancy. Each of the three leads is described as a reservoir of itinerant electrons in thermal equilibrium \(H_r = \sum_{r \in \{L,M,R\}} H_{T,r}\) connecting the four subsystems by spin-conserving tunneling between dot and leads

\[
H_{T,r} = \sum_{\alpha,\sigma} V_{r,\alpha,\sigma} c^\dagger_{\alpha,\sigma} c_{\alpha,\sigma} + H.c. \tag{2}
\]

The tunnel matrix elements \(V_{r,\alpha,\sigma} = t_r (\alpha | e^{-i \sigma_r \phi_r} e^{-i \sigma_y \theta_r} | \sigma)\) consist of the (spin-independent) tunnel amplitude \(t_r\), which is a measure of the barrier height and thickness, times an \(SU(2)\) rotation about the relative polar angles \(\theta_r\) and \(\phi_r\) between the lead’s magnetization direction and the dot’s spin quantization axis. The tunneling rate for electrons from lead \(r\) with spin \(\pm\) is quantified by \(\Gamma_r^{\pm}/\hbar = 2\pi |t_r^\dagger| \rho_r^{\pm}/\hbar\), and we define \(\Gamma_r = (\Gamma_r^+ + \Gamma_r^-)/2\). The system considered in this paper extends the quantum-dot spin valve studied in Ref. 22 by the addition of a third (base) electrode. We choose this lead to be floating, i.e., to carry no electric charge current. Instead, it influences the quantum-dot spin, and thus the source-drain current, only by magnetic interactions.

The state of the quantum dot is characterized by the probabilities \(P_{\chi}\) to find the dot empty \((\chi = 0)\), singly \((\chi = 1)\), or doubly \((\chi = d)\) occupied, as well as the average spin \(\hbar S\) with \(S = (S_x, S_y, S_z)\). We restrict ourselves to the limit of weak tunnel coupling, for which each tunnel event can be uniquely attributed to one lead. Therefore the kinetic equations of a quantum dot with three connecting leads appears identical to the two-lead case, whereby the sum over the leads has to be extended to include also the base (middle) lead. In lowest order in the tunnel coupling \(\Gamma_r\), the kinetic equations read

\[
\frac{d}{dt} \begin{pmatrix} P_0 \\ P_1 \\ P_d \end{pmatrix} = \sum_{r=L,M,R} \Gamma_r \begin{pmatrix} -2f_r^+ (\varepsilon) & f_r^- (\varepsilon) & 0 \\ 2f_r^+ (\varepsilon) & -f_r^- (\varepsilon) - f_r^+ (\varepsilon + U) & 0 \\ 0 & 2f_r^- (\varepsilon + U) & 0 \end{pmatrix} \begin{pmatrix} P_0 \\ P_1 \\ P_d \end{pmatrix} + 2 \begin{pmatrix} f_r^- (\varepsilon) + f_r^+ (\varepsilon + U) \\ f_r^- (\varepsilon + U) - f_r^+ (\varepsilon + U) \end{pmatrix} \begin{pmatrix} 0 \\ f_r^- (\varepsilon) + f_r^+ (\varepsilon + U) \end{pmatrix} \begin{pmatrix} -1 \\ 0 \\ 1 \end{pmatrix} \cdot \begin{pmatrix} S_x \\ S_y \\ S_z \end{pmatrix}, \tag{3}
\]

for the occupation probabilities of the different charge states, while the spin degrees of freedom are determined by

\[
\frac{dS}{dt} = \sum_{r=L,M,R} \Gamma_r \left( f_r^+ (\varepsilon) P_0 + \frac{-f_r^- (\varepsilon) + f_r^+ (\varepsilon + U)}{2} P_1 - f_r^- (\varepsilon + U) P_d \right). \tag{4}
\]

The kinetic equation \(\alpha\) contains a term describing coherent spin precession about an effective magnetic field, mediated by tunneling between dot and leads

\[
B_r = \frac{1}{\hbar} p_r \frac{1}{\pi} \int d\omega \Gamma_r (\omega) \left( \frac{f_r^+ (\omega)}{\hbar \omega - \varepsilon - U} + \frac{f_r^- (\omega)}{\hbar \omega - \varepsilon} \right), \tag{5}
\]

where the prime on the integral symbolizes Cauchy’s principal value. In this paper we consider the case of flat bands such that \(\Gamma_r\) is independent of \(\omega\) and the exchange field Eq. \(\alpha\) vanishes in the absence of charging energy.

By solving the system of kinetic equations \(\alpha\) and \(\beta\) in the stationary limit (under the constraint of probability normalization) we obtain the charge and spin occupation probabilities \(P\) and \(S\). The stationary charge current into lead \(r\) is then given by

\[
I_r = \frac{2(-\varepsilon) \Gamma_r}{\hbar} \left( f_r^+ (\varepsilon) P_0 + \frac{-f_r^- (\varepsilon) + f_r^+ (\varepsilon + U)}{2} P_1 - f_r^- (\varepsilon + U) P_d - \left[f_r^- (\varepsilon) + f_r^+ (\varepsilon + U)\right] \begin{pmatrix} S_x \\ S_y \\ S_z \end{pmatrix} \cdot p_r \right) \tag{6}
\]

We see that the quantum-dot charge and spin degrees of freedom are coupled to each other, and both enter the expression for the stationary current. In particular, an accumulation of spin in the quantum dot due to a finite source-drain voltage will reduce electric transport, which constitutes the spin valve effect.

The goal of this paper is to study how transport through this spin valve can be controlled in a purely magnetic way by means of the third lead. In order for this...
control to be purely magnetic we keep the base electrode floating, i.e., it does not carry any net charge current, \( I_M = 0 \).

The base lead influences the quantum-dot spin in two qualitatively different ways. First, the base electrode can act as (incoherent) sink for spin currents, thus offering a channel of spin relaxation. Second, the exchange field originating from the tunnel contact can give rise to coherent precession of the quantum-dot spin. Both effects could lead to a transistorlike behavior as discussed in the next section.

### III. QUANTUM-DOT SPIN TRANSISTOR

In this section we concentrate on the quantum-dot spin transistor as shown in Fig. 11. Source and drain electrodes are magnetized antiparallel to each other. This maximizes the magnitude of the accumulated spin on the quantum dot. The magnetization direction of the base electrode encloses an angle \( \theta \) with the source electrode. We are interested in the dependence of the source-drain current on the angle \( \theta \).

For simplicity we assume equal tunnel couplings \( \Gamma_L = \Gamma_R = \Gamma \) and polarizations \( p_L = p_R = p \) of the source and drain electrodes. Furthermore, we apply the transport voltage \( V \) symmetrically, \( V_L = -V_R = V/2 \), and focus on the linear-response conductance \( G = \partial I/\partial V \) for source-drain voltages \( eV \ll k_B T \) much smaller than the temperature.

In this case, the conductance can be expressed in terms of typical time scales that determine the quantum-dot charge and spin dynamics. The characteristic time scale of charge transport, \( \tau_c \), is the lifetime of the singly occupied charge state, limited by tunneling out of the dot or tunneling in of a second electron to or from the source or drain lead,

\[
\frac{1}{\tau_c} = \frac{2\Gamma}{\hbar} \left[ f^- (\varepsilon) + f^+ (\varepsilon + U) \right].
\]

This time scale directly reflects the electrical current through the quantum dot: in the absence of a source and drain lead polarization we would obtain the linear conductance \( G = \partial I/\partial V \) as

\[
G_0 = \frac{\varepsilon^2}{\hbar k_B T} \frac{1}{\tau_c} P_1^{(0)}.
\]

The conductance is directly proportional to \( 1/\tau_c \) times the equilibrium probability to find the dot singly occupied, \( P_1^{(0)} = 2 f^+ (\varepsilon) f^- (\varepsilon + U) / [ f^+ (\varepsilon) + f^- (\varepsilon + U) ] \).

The time scale for spin transfer or spin coherence is somewhat more subtle. Tunneling processes from or to ferromagnetic leads generate a finite spin accumulation as well as offering relaxation channels, which limit the spin lifetime. In Ref. 22 we chose to call the first and second terms in Eq. (4) the accumulation and relaxation terms, respectively. For the source and drain leads we keep this interpretation. The separation of the tunneling processes into spin accumulation and relaxation terms is to some degree arbitrary. To define a proper spin lifetime boundary conditions need to be specified. In the case of the base lead, the condition \( I_M = 0 \) allows us to rewrite the contribution of the middle (base) lead \( M \) to the spin kinetic equation (4) as

\[
\frac{d\mathbf{S}}{dt} |_M = -\frac{\Gamma_M}{\hbar} \left[ f^- (\varepsilon) + f^+ (\varepsilon + U) \right] \left[ \mathbf{S} - (\mathbf{S} \cdot \mathbf{p}_M) \mathbf{p}_M \right] + \mathbf{S} \times \mathbf{B}_M. \tag{9}
\]

By removing the spin-accumulation term from the kinetic equation we observe that the damping becomes anisotropic. Putting these pieces together leads to the definition of a spin lifetime

\[
\frac{1}{\tau_{s\parallel}} = \frac{2\Gamma + (1 - p_M^2)\Gamma_M}{\hbar} \left[ f^- (\varepsilon) + f^+ (\varepsilon + U) \right], \tag{10}
\]

for the case when the magnetization of the base lead is parallel to source and drain leads. For orthogonal alignment the spin lifetime becomes

\[
\frac{1}{\tau_{s\perp}} = \frac{2\Gamma + \Gamma_M}{\hbar} \left[ f^- (\varepsilon) + f^+ (\varepsilon + U) \right]. \tag{11}
\]

If the source and drain have a finite polarization \( p \), an average spin accumulates on the dot, giving rise to a magnetoresistive effect which reduces the conductance proportional to \( p^2 \). In the case of parallel source and base magnetizations (\( \theta = 0 \)) the base magnetization is also parallel to the accumulated spin. Due to this collinearity the precession term in Eq. (11) vanishes and the conductance \( G_{\parallel} \) is reduced to

\[
G_{\parallel} = G_0 \left( 1 - \frac{\tau_{s\parallel}}{\tau_c} p^2 \right). \tag{12}
\]

The characteristic charge transport time \( \tau_c \) is independent of the base lead as it is floating. In contrast the base lead may carry spin currents and thus reduce the spin lifetime \( \tau_{s\perp} < \tau_c \).

In the case of perpendicular magnetization alignment \( \theta = \pi/2 \), the intrinsic coherent spin precession also becomes important. In the stationary situation the electrical currents through source and drain interface are equal, therefore we may focus on the dot-drain interface only. This interface can be seen as a tunnel magnetoresistance element of its own, i.e., its conductance depends on the relative angle between dot spin \( \mathbf{S} \) and lead magnetization \( \mathbf{p}_F \). Since the exchange field originating from the base lead modifies the dot-spin direction, it also modifies the conductance of the device.\(^{22}\) In the orthogonal magnetization alignment the spin precession effect is maximally pronounced, and the magnetoresistance of the total device is reduced by the factor \( 1/(B_M^2 \tau_s^2 + 1) \) to

\[
G_{\perp} = G_0 \left( 1 - \frac{\tau_{s\perp}}{\tau_c} p^2 \frac{1}{B_M^2 \tau_s^2 + 1} \right). \tag{13}
\]
In Fig. 2 we plot the normalized conductance change $\Delta = (G(0) - G_{||})/G_{||}$ of the transistor structure as a function of the base lead magnetization direction. For $\theta = \pi/2$, the device conductance is maximal, since in this alignment both the spin relaxation due to the base lead and the spin-precession effect maximally suppress the magnetoresistance caused by spin accumulation. By comparison with the dashed curve, for which the exchange field was set to zero manually, it can be seen that the transistor shows significant influence of the exchange interaction which is caused by electron-electron interaction.

In Fig. 2(a), the maximum value of $\Delta(\theta = \pi/2)$ is plotted as a function of gate voltage. $\Delta$ shows strong variations, which arise only due to the gate-voltage dependence of the exchange field from the base lead [Fig. 2(b)]. Without the exchange interaction, no gate-voltage dependence is expected (see dashed line). Due to its strong gate-voltage dependence, the exchange interaction contribution can be separated from the influence of the anisotropic spin-flip relaxation, which does not depend as strongly on the gate voltage.

IV. ORTHOGONAL MAGNETIZATION

In the quantum-dot spin transistor geometry shown in Fig. 1 and discussed in the previous section, both spin-flip and spin-precession processes contribute at the same time. In the last part of this paper, we want to isolate the exchange-field contribution in a purely magnetic way.

For this, we consider a geometry of the quantum-dot spin transistor with pairwise orthogonal magnetization directions in the non-linear response regime (see Fig. 3). There are two realizations of such a system, defined by $p_L \cdot (p_M \times p_R) \leq 0$. They are related by reversal of the base magnetization or reversal of the voltage (and thus current directions). For these systems the anisotropic damping is equal, as it gives rise only to factors $1 - p_M^2$. Any difference in the transport behavior of the two systems can thus be attributed entirely to exchange effects.

The exchange field now always has contributions from all three leads, as source and drain contributions never cancel each other. Correspondingly, the axis and angle of precession of the dot spin depends on all three lead potentials and is not easily visualized, in particular in the case of finite bias voltages.

In the linear-response regime the conductances of the left- (LHS) and right-handed system (RHS) are equal to each other. This is a consequence of the symmetry of the system for equal source and drain parameters ($p_L = p_R$, $\Gamma_L = \Gamma_R$) (see Fig. 4).

In order to observe a difference in the conductances of the LHS and RHS, the symmetry of source and drain has to be broken, which is best done by application of finite bias voltages (Fig. 3). If the exchange fields are set to zero manually in the kinetic equations, a mechanism similar to the one described in Ref. 22 leads, for $p \rightarrow 1$, to complete spin blockade between $\varepsilon$ and $\varepsilon + U$: driven by the current,
the accumulated spin tends to align antiparallel to the drain electrode and thus blocks transport (dot-dashed line). In the presence of an exchange field this blockade is lifted due to precession of the accumulated spin. This process differs for the left- and right-handed systems due to the different precession directions, which are reflected in different conductances.

V. CONCLUSION

We analyzed electron transport through a magnetically controlled quantum-dot spin transistor in the regime of weak dot-lead tunnel coupling. The presence of Coulomb interaction on the dot gives rise to an exchange interaction of the accumulated dot spin with the ferromagnetic leads, giving rise to spin precession. Furthermore, the tunnel coupling to a current-free ferromagnetic base electrode leads to an anisotropic spin relaxation: dot spins oriented along this lead’s magnetization experience a weakened damping, i.e., an increased spin lifetime relative to other spin orientations.

These two effects allow for a purely magnetic control of the source-drain current. We demonstrated this for two setups. In the first, with source and drain magnetized antiparallel to each other, we found a dependence of the source-drain voltage on the magnetization direction of the base lead. The influence of the exchange field becomes clearly visible in the gate-voltage dependence of the conductances, allowing for the possibility of separating the two effects in experiments. As a second possibility to isolate the exchange-field contribution we propose a setup with all three leads’ magnetizations being pairwise orthogonal to each other. In this case the difference of the currents for the left- and right-handed systems is purely due to the exchange field.

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APPENDIX A: EXCHANGE FIELD AND SPIN-MIXING CONDUCTANCE

The accumulated spin $S$ on the quantum dot is coupled to the magnetization of the ferromagnetic lead via virtual tunnel processes. This coupling leads to a precession of the dot spin around the lead magnetization direction, described by the exchange field $B$ in Eq. (5). In terms of angular momentum transfer the precession is equivalent to a spin current transverse to both lead magnetization and dot spin-accumulation direction. The transversal is directly reflected in the cross-product structure ($S \times B$) in Eq. (4).

For noninteracting systems, spin transport through interfaces has been studied extensively in terms of a scattering-wave approach. Brataas et al. found that spin transport can be characterized by three parameters: the conductance for spin-up electrons, that for spin-down electrons, and the complex spin-mixing conductance

$$G_{\uparrow \downarrow}^{\uparrow \downarrow}(\omega) = \frac{e}{h} [1 - r_{\uparrow \downarrow}(r_{\downarrow \uparrow})^*], \quad (A1)$$
where $r_{\sigma\sigma}$ are the reflection amplitudes of electrons with spin $\sigma$ and energy $\omega$. Electrons entering the junction from the normal side and being reflected at the interface acquire a spin-dependent phase shift, equivalent to a rotation of the spin state about the magnetization direction of the ferromagnet. This mechanism, also discussed in the context of singlet-triplet mixing in ferromagnet-superconductor heterostructures, is described by the imaginary part of the spin-mixing conductance and leads to a transverse component of the spin current through an interface.

We now show how the exchange field that we calculate in terms of Green’s functions can, for the noninteracting limit $U = 0$, be matched to the imaginary part of the spin-mixing conductance. For this we consider an electron arriving from the ferromagnet, which scatters back at the ferromagnet–quantum-dot interface by means of the Fisher-Lee relations. We can relate the reflection amplitude

$$r_{\sigma\sigma}(\omega) = -1 + i\Gamma_{\sigma}(\omega)G_{\sigma\sigma}^{\text{ret}}(\omega)$$

(A2)

to the retarded Green’s function $G_{\sigma\sigma}^{\text{ret}}(\omega)$ of the quantum dot and the spin-dependent tunnel coupling $\Gamma_{\sigma}$, which yields

$$G_{\uparrow\uparrow}^{\text{ret}}(\omega) = \frac{ie}{\hbar} (\Gamma_{\uparrow} G_{\uparrow\uparrow}^{\text{ret}} - \Gamma_{\downarrow} G_{\downarrow\downarrow}^{\text{ret}}) = \frac{e}{\hbar} (\Gamma_{\uparrow} + \Gamma_{\downarrow}) (-\text{Im} G_{\sigma\sigma}^{\text{ret}} + i\nu \text{Re} G_{\sigma\sigma}^{\text{ret}})$$

(A3)

plus terms of higher order in $\Gamma$. In the last line, we dropped the spin indices on the Green’s functions, as in the limit of zeroth order in $\Gamma$, the diagonal Green’s functions $G_{\sigma\sigma}^{\text{ret}}(\omega) = 1/(\omega - \varepsilon + i0^+)$. are independent of spin.

At this point, we can identify two conceptually different contributions to the spin mixing conductance: the real part of the conductance is proportional to the spectral density of the quantum dot, associated with a real particle transfer between lead and dot. On the other hand, the imaginary part of the mixing conductance is proportional to the polarization $\sigma = (\Gamma_{\uparrow} - \Gamma_{\downarrow})/(\Gamma_{\uparrow} + \Gamma_{\downarrow})$ and to $\text{Re} G_{\sigma\sigma}^{\text{ret}}$. To get the total transfer of angular momentum between dot and lead, we need to integrate over all frequencies $\omega$, which gives rise to a principal value integral with integrand $1/(\omega - \varepsilon)$, in agreement with a full Green’s function formulation of the spin current through a tunnel barrier.

Eventually, we find the resulting integral equal to the expression of the exchange field $B_z$ in Eq. (5) in the noninteracting limit $U = 0$,

$$\int d\omega \text{Im} G_{\uparrow\uparrow}^{\text{ret}}(\omega) = 2e |B_z|$$

(A4)

This result complements the scattering picture, within which the spin-mixing conductance emerges from the shape of the interface barriers. Such structural aspects are not accessible within the Green’s function formalism employed in this paper, since the underlying Hamiltonian describes high and narrow barriers. The scattering wave approach, on the other hand, is unable to describe many-particle effects such as the exchange field. While both contributions are present in the spin-mixing conductance, it depends on the specific system which one dominates.

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This approach requires the vanishing of the dot Green’s functions nondiagonal in spin space, which is always satisfied in the weak-coupling limit.
It is worth mentioning that the retarded and advanced zeroth-order Green’s functions of the dot electrons are formally equal to the free Green’s functions, even though this is not the same limit. The zeroth-order approximation takes into account fully the nonequilibrium situation of the system. This point becomes more transparent by considering that the off-diagonal greater and lesser Green’s functions vanish in the free limit, while in zeroth-order tunnel coupling Γ they do not, but rather describe nonequilibrium spin accumulation on the quantum dot.
M. Braun, J. König, and J. Martinek, Superlattices Microstruct. 37, 333 (2005).