Supplement of

Improved tropospheric and stratospheric sulfur cycle in the aerosol–chemistry–climate model SOCOL-AERv2

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Figure S1: The liquid fraction of clouds in the mixed-phase cloud regime ($-38 \, ^\circ C < T < 0 \, ^\circ C$) simulated by SOCOL-AERv1 based on ECHAM5 during a one-year simulation (solid circles). 12-hourly model output in all grid boxes with clouds is averaged in 1 degree temperature bins, with standard deviation bars included. The red curve shows the fitted sigmoid function (Hu et al., 2010) for the supercooled liquid fraction, $\text{SLF}_{\text{Hu}}$, derived from CALIOP Lidar measurements on board of the CALIPSO satellite. In its aqueous chemistry scheme, SOCOL-AERv2 adopts the satellite SLF to calculate the liquid water content from the model’s total water content, $\text{LWC} = \text{SLF}_{\text{Hu}} \times \text{TWC}$. 

![Graph showing the liquid fraction of clouds versus temperature]
Figure S2: Comparison between annual mean model extinctions at 525 and 1020 nm and SAGE II measurements from the GloSSAC project (Thomason et al., 2018) at the Equator (top) and 45° N (bottom). Observations are averaged between 2000–2004, representing the volcanically quiescent part of the record. Model results are averaged over 5 years of the year 2000 time-slice for SOCOL-AERv2, ICE_OX, and AER_SCAV. Horizontal bars represent the modelled or observed standard deviation. The highlighted region in the upper plot corresponds to the altitudes where non-sulfate aerosols may play a role.
Figure S3: Number densities of particle size bins measured by OPC (Deshler et al., 2003; Deshler, 2008) and modelled by ICEOX and AER_SCAV over Laramie, Wyoming, USA (41° N, 105° W) and Lauder, New Zealand (45° S, 170° W). Measured number densities are shown as box plots (minimum excluding outliers below the 0.4 percentile, 25th percentile, median, 75th percentile, maximum excluding outliers above the 99.6 percentile) and modelled number densities as solid lines. For the Laramie plots (left), OPC measurements are used from the period 1999–2008 and zonal mean model results are averaged over the 5 years of the time-slice. For the Lauder plots (right), OPC measurements are used from January to April 1998–2001 and zonal mean model results are averaged from January to April over 5 years of the time-slice. Model results are weighted with the counting efficiencies for OPC channels from Deshler et al. (2019) for direct comparability with the measurements.
Figure S4: Comparison of modelled biases, relative to measurement sites from the WMO database (Vet et al., 2014), in precipitation and deposition. SOCOL-AERv2 is compared with measurements in two different time periods, 2000–2002 and 2005–2007. The Spearman correlation coefficient is listed on each plot.
Figure S5: Evaluation of modelled SO$_2$ dry deposition against North American measurement sites from the WMO database (Vet et al., 2014). SOCOL-AERv1 and SOCOL-AERv2 are compared with measurements in two different time periods, 2000–2002 and 2005–2007. The ensemble standard deviation for the model results is shown as vertical bars. A power regression between the simulation results and measurements is shown in blue, and can be compared to the one-to-one line shown in black. Two model evaluation metrics are listed on the plots: the goodness of fit of the power regression between model and measurements ($R^2$) and the fraction of sites for which the model is within a factor of 2 of measurements ($f_{2x}$). Points are colored according to the measurement network of the sites.
**Figure S6:** Evaluation of modelled sulfate aerosol dry deposition against North American measurement sites from the WMO database (Vet et al., 2014). SOCOL-AERv1 and SOCOL-AERv2 are compared with measurements in two different time periods, 2000–2002 and 2005–2007. The ensemble standard deviation for the model results is shown as vertical bars. A power regression between the simulation results and measurements is shown in blue, and can be compared to the one-to-one line shown in black. Two model evaluation metrics are listed on the plots: the goodness of fit of the power regression between model and measurements ($R^2$) and the fraction of sites for which the model is within a factor of 2 of measurements ($f_{2x}$). Points are colored according to the measurement network of the sites.

**Table S1:** The time periods covered by model intercomparison projects of sulfur deposition and this study.

| Project Name | Simulation Period | Observation Period | Reference          |
|--------------|-------------------|--------------------|--------------------|
| Photocomp    | 2000              | 2000               | Dentener et al. (2006) |
| ACCMIP       | 2000              | 2000–2002          | Lamarque et al. (2013) |
| HTAP I       | 2001              | 2000–2002          | Vet et al. (2014)   |
| HTAP II      | 2010              | 2009–2011          | Tan et al. (2018)   |
| SOCOL-AERv2  | 2000–2002         | 2000–2002          | This study          |
|              |                   | 2000–2002          |                    |
|              |                   | 2005–2007          |                    |
S1 References

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