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Laser-cooled polyatomic molecules for improved electron electric dipole moment searches

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Abstract

Doppler and Sisyphus cooling of 174YbOH are achieved and studied. This polyatomic molecule has high sensitivity to physics beyond the Standard Model and represents a new class of species for future high-precision probes of new T-violating physics. The transverse temperature of the YbOH beam is reduced by nearly two orders of magnitude to < 600 μK and the phase-space density is increased by a factor of > 6 via Sisyphus cooling. We develop a full numerical model of the laser cooling of YbOH and find excellent agreement with the data. We project that laser cooling and magneto-optical trapping of long-lived samples of YbOH molecules are within reach and these will allow a high sensitivity probe of the electric dipole moment of the electron. The approach demonstrated here is easily generalized to other isotopologues of YbOH that have enhanced sensitivity to other symmetry-violating electromagnetic moments.

1. Introduction

Experimental probes of the electric dipole moment of the electron (eEDM) provide strong constraints on theories of particle physics beyond the Standard Model (BSM) [1–6]. The most stringent limit on an eEDM has been realized in experiments using a diatomic molecule, ThO, in a 3Δ1 state, limiting the eEDM to < 1.1 × 10−29 e cm [7, 8]. This has placed limits on T-violating new physics above the TeV scale [5, 6]. Other work, using HfF5 with the same electronic structure, has confirmed the ACME results at the < 1.3 × 10−28 e cm level [9]. The sensitivity of these experiments comes in part from the particular structure of the angular momentum states in these molecules. Specifically, orbital angular momentum along the internuclear axis allows one to fully polarize the molecules in the lab frame, thereby providing control of the large internal effective electric field (> 10–100 GV cm−1) [10, 11]. For these two molecules, this structure and concomitant ease of polarization, which is the result of closely spaced levels of opposite parity in Ω-doublet states, allows for strong rejection of many systematic errors [12]. A future eEDM search could combine this internal structural feature with other advances, such as extended coherence times and larger numbers of molecules. It was recently proposed [13] that polyatomic molecules generically allow for eEDM searches that combine scalability, polarizability, long coherence times, and robustness to systematic errors. In particular, YbOH was pointed out as a viable candidate for greatly improved searches of symmetry-violating new physics. Other heavy polyatomic molecules, such as RaOH [14] and ThOH+ and RaOH+ [15], are also expected to have enhanced sensitivity to T-violating physics. Polyatomic molecules are also of interest to other tests of BSM physics, often due to vibrational modes which have no analogs in diatomic species. For example, degenerate bending modes can provide avoided crossings useful in probing nuclear spin-dependent parity violation [16], tunneling [17, 18] and torsional [19–21] transitions provide enhanced sensitivity to drifts in fundamental constants, and vibronic coupling can yield similar enhancement factors [22].
eEDM-sensitive molecules with nonzero angular momentum projection along the internuclear axis arising from electronic orbits, i.e. the highly polarizable $^3\Delta_1$ state, have very poor laser cooling properties [13]. No diatomic molecule with sensitivity to new physics has been identified that is simultaneously amenable to laser cooling while also providing convenient parity doublets for polarization and systematic error control. Polyatomic molecules, on the other hand, generically possess small parity doublets arising from nuclear orbital motion. For example, the low-lying bending modes of linear triatomic molecules in $^3\Sigma$ states possess nearly degenerate levels of opposite parity that are metastable. These levels, which are absent in diatomic species, can be fully polarized and allow internal comagnetometry, features which enable strong systematic error rejection. Thus, a class of molecules has been identified where a precision measurement with trapped polyatomic molecules, e.g. $^{174}$YbOH, could probe CP-violating BSM physics at the PeV scale in a near-term experiment [13, 23, 24]. Trapped molecules present many other practical advantages to future eEDM experiments. They offer robust systematic error rejection due to the ability to control external fields with exquisite precision over the small trap volumes involved. Furthermore, one may vary the precession time in order to eliminate systematic errors associated with state preparation.

In order to achieve long coherence times and manage systematic errors, trapping of molecules under weakly perturbing conditions and with long lifetimes, e.g. in an optical dipole trap (ODT), will be crucial in the pursuit of next-generation eEDM measurements. Weak traps require much lower molecule temperatures than were achieved in recent eEDM experiments, and therefore some form of deeper cooling is necessary. Direct laser cooling of molecules [25–29] has seen rapid growth in recent years; SrF [28, 30–36], GaF [37–42], and YO [43–45] have all been laser-slowed, cooled, and transferred to long-lived traps. YbF [46] molecules have been transversely laser-cooled, although not yet cooled in three dimensions. In experimental work begun in 2014, the polyatomic radical SrOH was sub-Doppler cooled in one dimension [47], marking a path to cooling of much heavier and more complex isoelectronic species, like YbOH. Foundational work [14] found that polyatomic molecules with heavy nuclei can have highly diagonal vibrational branching ratios, showing for the first time that eEDM-sensitive molecules could be laser cooled. To date, there has been no experimental demonstration of laser cooling of a polyatomic molecule with strongly enhanced sensitivity to the eEDM [48]. This is in part because heavy polyatomics, like YbOH, are significantly more challenging than previously cooled species due to their high masses, strong perturbations in the electronically excited states, and less favorable Franck–Condon factors.

We report here one-dimensional Doppler and Sisyphus cooling of a beam of $^{174}$YbOH from 20 $\mu$K to below 600 $\mu$K. The particular Sisyphus effect used here, called the magnetically-assisted Sisyphus effect, has been investigated previously in both atoms [49–51] and molecules [31, 46, 47]. Consistent with previous work on atoms and lighter molecular species, we observe that Sisyphus cooling is more efficient than Doppler cooling because the magnitude of the cooling force is set by the depth of the laser field’s light shifts, which can be made arbitrarily deep at high intensity [50, 52, 53]. The laser cooling demonstrated here is a crucial proof-of-principle test for further direct cooling and trapping of YbOH molecules for a new generation of eEDM experiments. We create a theoretical simulation based on the optical Bloch equations and find excellent agreement with our experimental data. We discuss extensions of our approach to isotopologues of YbOH, including $^{173}$YbOH, which have been proposed for use in measurements of the nuclear magnetic quadrupole moment [54].

2. Experiment

Figure 1(a) shows a schematic diagram of the experimental apparatus. YbOH molecules are produced in a cryogenic buffer-gas beam (CBGB) [55, 56], the essential approach used in all molecular laser cooling experiments. A cryogenic cell is held at ~2 K and filled with $^4$He buffer-gas. Hot methanol gas (~250K) is flowed into the cell through a thermally isolated capillary. Laser ablation of Yb metal, followed by a chemical reaction between the Yb atoms and methanol, produces YbOH molecules that are cooled by the He buffer gas. YbOH molecules entrained in the He buffer gas are then extracted into a beam. A typical He flow of 3 sccm is used and the molecules are extracted from the cell through a 16 mm × 2.4 mm slit (vertical × horizontal). A typical YbOH CBGB contains ~$10^6$ YbOH molecules in the $N'' = 1$ rotational level, as measured via absorption spectroscopy. The mean forward velocity is $v_f \sim 90$ m s$^{-1}$ and the transverse velocity spread is $v_t \sim 15$ m s$^{-1}$. A 2.7 mm × 3 mm aperture placed 20 cm downstream from the cell collimates the molecular beam to an effective transverse temperature of $T_t \sim 20$ mK.

Just after the aperture, the molecules enter a cooling region of variable length up to $L_{\text{int}} \sim 50$ mm (interaction time $t_{\text{int}} \sim 500 \mu$s). The cooling region contains light at four different wavelengths. The main photon cycling transition is $\tilde{A}$ $^3\Pi$(000) $\leftrightarrow$ $\tilde{X}$ $^3\Sigma^+$ (000) (577 nm) [58, 59]. Significant optical pumping into higher lying vibrational states occurs. Linear triatomic molecules possess three vibrational modes: the symmetric stretch, antisymmetric stretch, and doubly degenerate bend. We label the vibrational levels using the
notation \((v_1, v_2, v_3)\), where \(v_1\) indicates the number of quanta of excitation in the symmetric stretching mode, \(v_2\) the quanta in the bending mode, and \(v_3\) the quanta in the antisymmetric stretching mode. \(\ell\) labels the excitation of nuclear orbital angular momentum in the bending mode. In the present work, dominant decays are to the \(S^+ X^{000}\), \(200\), and \(020\) levels, and vibrational repumping is required to return this population to the main cooling cycle. The vibrational branching ratios from the \(A^{000}\) state will be the focus of a future publication \cite{58}. Note that vibrational angular momentum selection rules strongly limit decays to the \(010\) bending mode \cite{60}. Thus, the cooling region also includes light to drive \(P \rightarrow S^+ A^{000} X^{1002}(\ell=0)\) (595 nm, ‘first repump’), \(A^2 \Pi(D=1) \rightarrow \tilde{X}^2 \Sigma^+(002)\) (599 nm, ‘second repump’), and \(17.73\) (000) \(\rightarrow \tilde{X}^2 \Sigma^+(200)\) (600 nm, ‘third repump’)\footnote{The \(17.73\) state is an electronically excited state present in YbOH. It behaves mostly like a \(\Pi_{1/2}\) state and, importantly for the laser cooling scheme, decays predominantly to the \(\tilde{X}^2 \Sigma^+(000)\) and (100) levels.}.

The magnetically-assisted Sisyphus effect has been described in detail previously \cite{50}. In brief, spatially-varying light shifts, optical pumping into dark magnetic sublevels, and remixing by a static magnetic field lead to an effective friction force which can be much larger than typical Doppler cooling forces. Due to the angular momentum structure of the YbOH transitions used here, we expect cooling at blue detuning and heating at red detuning. To produce the cooling force, the main and first repump laser beams propagate perpendicular to the molecular beam making 12 round-trip passes between mirrors to create a standing wave. Each beam has diameter \(\sim 4\) mm. A variable magnetic field is present in the cooling region to provide the remixing between dark and bright states necessary for the magnetically-assisted Sisyphus effect \cite{50,61}. The field is oriented at 45 degrees to the cooling light’s polarization axis to ensure near-optimal remixing. The magnetic field is typically \(\sim 1.5\) Gauss, as this leads to a Larmor precession time roughly matching the molecular transit time between a node and antinode of the standing wave \cite{46}. In the case of Doppler cooling (as opposed to the Sisyphus configuration) the standing wave is purposely destroyed by misaligning the retro-reflected beams, but the
magnetic field is left on to remix any transient dark states. The second and third repump laser beams, of diameter 6 mm, enter the cooling region through separate fibers, cover the cooling region, and do not form standing waves. For both Doppler and Sisyphus cooling, the light from each laser is split into two frequency components separated by the spin-rotation (SR) splitting of the \( N'' = 1 \) state; these address the \( P_1(N'' = 1) \) and \( ^3Q_{12}(N'' = 1) \) lines [62] (see figure 1(b)). These transitions are rotationally closed, and have been used in all previous molecular laser cooling experiments.

The main cooling light at 577 nm is generated by the second harmonic of a Raman fiber amplifier, while all repumping and imaging wavelengths are generated by cw dye lasers. Up to 150 mW of main cooling light, 100 mW of (100) repumping light, and 50 mW of (200) and (020) repumping light are incident on the molecules from each direction. The SR structure in the \( \tilde{X} \ 3\Sigma^+ \) state, which arises from interaction with \( \Omega = 1/2 \) excited electronic states, is unusual because the splitting scales quickly with vibrational level (see figure 1(c)). The same effect has been observed in YbF and is attributed to competing contributions from the \( \tilde{A} \ 4\Pi_{1/2} \) vibrational states and vibrational levels of \( \Omega = 1/2 \) excited electronic states arising from an Yb\(^+\) \((f^{13})\) configuration [57, 63–66]. To address both SR components, we pass each laser beam through an acousto-optic modulator (AOM) which adds a frequency sideband at the appropriate rf interval. The proton hyperfine splittings in \( ^{17}\text{YbOH} \) are unresolved in optical excitation (<3 MHz, see figure 1(b)). The splittings are small due to the large distance between the hydrogen nucleus and the predominantly metal-centered valence electron [57].

After the cooling region, the molecules travel 40 cm in free flight and then encounter clean-up and imaging regions. In the ‘clean-up’ region only the (200) and (020) repumping light is present in order to return any population in excited vibrational states back to the lowest vibrational levels in preparation for imaging via laser-induced fluorescence (LIF). In the imaging region, the molecular beam is imaged with an EMCCD by driving the \( \tilde{A}(000) \leftarrow \tilde{X}(000) \) and \( \tilde{A}(000) \leftarrow \tilde{X}(100) \) transitions and collecting LIF at 577 nm. The imaging light contains 10 mW of main line and 40 mW of (100) repumping light. The detection light is always resonant and retro-reflected in order to avoid systematic effects due to Doppler shifts in the imaging light. The imaging system is calibrated to ensure that the magnification and collection efficiency are roughly uniform over the entire field of view of 22 mm.

3. Results and discussion

A typical set of EMCCD images under Sisyphus conditions, expected to give heating at red detuning and cooling at blue detuning [50], is shown in figure 2. Figure 2(a) shows a typical molecular beam image when the lasers in the cooling region are all tuned to resonance. At the highest intensities \( (I/I_{sat} \sim 70) \) roughly 40% of the molecules remain for detection. The loss is attributed to decays to both the \( \tilde{X}(300) \) and \( \tilde{X}(00^0) \) levels, whose precise energies are unknown. The branching ratios to both states are known, however, and the loss allows us to calibrate the number of photons scattered per molecule. Using the measured branching ratios, \( 1.0(0.25) \times 10^{-3} \) to the \( \tilde{X}(300) \) level and \( 0.8(3) \times 10^{-2} \) to the \( \tilde{X}(00^0) \) level [67], we determine that the molecules scatter an average of \( 500^{\pm 300} \) photons. The scattering rate is measured independently, via images of fluorescence over the molecules’ path, to be \( \Gamma_c \approx 1.5 \times 10^6 \text{s}^{-1} \). This is consistent with the estimated number of photons scattered as determined by loss to dark states.
In figure 2(b) (and figure 2(c)), the molecular beam is imaged after passing through a cooling region with light detuned by 1.8Γ to the red (and blue) of resonance. (Γ = 1/τ = 2π × 9 MHz.) At Δ = −1.8Γ there is a clear heating feature indicated by expulsion of population from the central beam axis. At Δ = +1.8Γ the molecules are cooled and collimated, which results in an increase in on-axis density. Integrating across the central region of these images results in figure 3(a). We note that Sisyphus heating concentrates population at specific nonzero velocities. This is because Sisyphus heating is operative at red detuning, but only over a small range of velocities. The Doppler forces become dominant beyond the capture velocity of the Sisyphus force, and population accumulates at the velocity for which these forces balance. This allows us to estimate a value for the capture velocity of the Sisyphus effect of approximately 1 m s\(^{-1}\) at \(I/I_{\text{sat}} \sim 65\). As discussed below, this is in good agreement with our theoretical model.

In order to interpret the integrated images we fit the transverse beam profiles to a set of Gaussians. The resonance condition molecular beam profile (figure 3(a)) is first fit to a single Gaussian. In all experimental conditions it is found that the width of the beam is unchanged if light is present in the cooling region but tuned to resonance; only the overall amplitude of the beam signal changes in this case. Next, the cooled beam profile (figure 3(b)) is fit to the sum of two Gaussians: one whose width is constrained to match the uncooled signal and another whose width is allowed to vary. In this way we capture the fact that not all molecules in the experiment are below the transverse capture velocity of the Sisyphus force. The relative areas under the ‘cooled’ and ‘uncooled’ portions give a measure of the fraction of molecules within the Sisyphus capture range. In our data the cooled portion of the beam typically contains up to 60% of the molecules. This is consistent with the capture velocity estimated above and the expected velocity distribution produced by the collimating aperture. At maximum intensity, the Sisyphus cooling configuration reduces the FWHM of the cooled molecular beam from 8.5(5) mm to 3.0(4) mm.

By misaligning the retro-reflected laser beams by ~2 beam waists to remove the standing wave condition in the cooling region, we are also able to exclusively study Doppler cooling of the molecular beam. The fitted beam widths as a function of laser detuning are shown in figure 4(a), which are collected at the same magnetic field (\(B \sim 1.5\) G) and with the same number of photons scattered (~500) as for Sisyphus cooling. In contrast to Sisyphus cooling, the Doppler scan shows cooling at red detuning and heating at blue detuning. The Doppler cooling and heating are efficient over a large range of frequencies due to the power broadening at the high intensities used in this study. The overall magnitude of the cooling and heating forces are significantly smaller in the Doppler configuration than in the Sisyphus configuration. This is due to the large light shifts present in the molasses, as described below.

In the Sisyphus configuration, we expect the transverse temperature to decrease as the standing wave intensity is increased, as shown in figure 4(b). The data shows a clear saturation of the minimum beam width at a size set by the collimating aperture, i.e. the molecules expand negligibly during the 40 cm of free flight following this aperture. In order to fit the images to a transverse temperature, we follow [47] in comparing the beam width after the cooling region to a Monte Carlo model of ballistic expansion. This yields a minimum temperature of 500±100 μK. The temperature has large and asymmetric error bars because the cooled beam is close to the size of the 3 mm collimating aperture, so fitting the cooled cloud size yields very limited temperature resolution. At this temperature, the uncertainty of the fit is comparable to the central value, such that we can only place an upper limit on the temperature. We therefore interpret the extracted temperature as a bound, \(T_L < 600\) μK. Because there is no fundamental temperature limit to the Sisyphus cooling near this scale, the actual temperature is likely much lower; this is discussed in more detail below, where we present the results of calculations using the optical Bloch equations. Figure 4(c) shows the fraction of the molecular beam that has been cooled. The value increases with intensity to approximately 60% at \(I/I_{\text{sat}} \sim 65\), and is not yet saturated at the intensities explored in this
work. Given the spread of velocities in the unperturbed molecular beam, this value of the cooled fraction is consistent with the estimated capture velocity of \( \sim 1 \text{ m s}^{-1} \). From this cooled fraction, we estimate that around \( 5 \times 10^4 \) molecules are in the ultracold part of the distribution. Accounting for the loss to dark states and reduction in transverse temperature, this corresponds to an increase in phase-space density (PSD) in one dimension of a factor of 6.

We have constructed a detailed model of the laser cooling forces based on \( \text{[30, 68, 69]} \). Because the SR splittings are all large compared to the detunings in the experiment, the molecular beam width on Sisyphus cooling light intensity, at detuning \( \Delta = 1.5T \). The beam width initially decreases as the cooling intensity is increased, before saturating to a width set by the collimating aperture. Temperature resolution is limited to \( \sim 600 \text{ } \mu \text{K} \) in direct fits of the width. (c) Fraction of the beam within the ‘cold’ portion of the beam, as determined by our two-Gaussian fit. Data taken at \( \Delta = 1.3T \). In all plots, error bars on experimental points come from the spread in repeated measurements. Shaded regions represent the spread in simulation outputs when the simulated laser beam overlap in the cooling region is varied, as described in the main text.

![Figure 4](image-url)

**Figure 4.** (a) Comparison of Doppler and Sisyphus cooling as a function of detuning. Data taken at an intensity of \( I/I_{sat} \sim 15 \). The magnetically-assisted Sisyphus effect has the opposite detuning dependence and higher cooling efficiency when compared to Doppler cooling. (b) Dependence of the molecular beam width on Sisyphus cooling light intensity, at detuning \( \Delta = 1.5T \). The beam width initially decreases as the cooling intensity is increased, before saturating to a width set by the collimating aperture. Temperature resolution is limited to \( \sim 600 \text{ } \mu \text{K} \) in direct fits of the width. (c) Fraction of the beam within the ‘cold’ portion of the beam, as determined by our two-Gaussian fit. Data taken at \( \Delta = 1.3T \). In all plots, error bars on experimental points come from the spread in repeated measurements. Shaded regions represent the spread in simulation outputs when the simulated laser beam overlap in the cooling region is varied, as described in the main text.

\[ \hbar \sqrt{2 \pi m k_B T} \]

The phase-space density is given by \( n, \lambda_{\text{SR}, \lambda_{\text{SR}, \lambda_{\text{SR}}}} \), where \( n \) is the number density and \( \lambda_{\text{SR}, \lambda_{\text{SR}, \lambda_{\text{SR}}}} = h\sqrt{2\pi m k_B T} \) is the de Broglie wavelength for molecules with mass \( m \) and temperature \( T \). Because the cooling is only in one dimension, PSD scales with the square root of the temperature rather than \( T^{1/2} \).
4. Conclusion

In summary, we demonstrate Sisyphus and Doppler laser cooling of the polyatomic radical $^{174}$YbOH. Under Sisyphus conditions, the transverse temperature of the YbOH beam is reduced from $\sim 20$ mK to $< 600 \mu$K with $\sim 500$ photons scattered per molecule. Sisyphus cooling is found to be significantly more efficient (per photon scattered) than Doppler cooling, as expected due to the large light shifts induced by the near-resonant standing waves [47, 50]. We compare our results to simulations based on the optical Bloch equations and find agreement over a range of parameters. Validating this model is important as it can be used to guide future experiments to cool and trap YbOH and other molecules sensitive to BSM physics. Due to the expected optical pumping to unaddressed vibrational states, the on-axis density of the cooled molecular beam is approximately equal to the unperturbed beam. The decrease in temperature leads to an increase in the PSD around a factor of 6 under the very conservative assumption of $600 \mu$K for the transverse temperature of the cooled beam.

Our results are a proof-of-principle demonstration toward further laser cooling of YbOH samples to temperatures low enough for optical trapping. In addition, the transverse cooling demonstrated here could be extended to two dimensions, increasing the number of molecules in an optical trap. The temperature limits determined here are set by the number of photons scattered per molecule, which in turn is set by the number of vibrational repump lasers used in the experiment. This could be improved in future experiments. Measurements of the vibrational branching ratios to $X(300)$ and $X(0\text{I}^0\text{I})$ indicate that adding these two additional repumping lasers will increase the number of photon scatters per molecule to $\sim 3000$ before decay to other unaddressed vibrational levels (with higher vibrational quantum numbers) becomes a limiting factor$^6$. Adding two or three more repumping lasers would bring this figure to $> 10,000$ photons [70, 71], sufficient to produce a magneto-optical trap of YbOH. Additional excited electronic states, such as the $B\ 3\Sigma^+$ state, could also improve the laser cooling by providing additional repumping pathways. Spectroscopic and theoretical work to locate this state is therefore greatly motivated. Transverse Sisyphus cooling could also contribute directly to improvements in beam-based precision measurements by increasing the number of molecules probed while also allowing longer beam lines, and thus longer coherence times. Straightforward extension of the technique to $^{173}$YbOH would be useful for proposed nuclear magnetic quadrupole moment measurements [13, 54]. A more complex repumping scheme will be required in this case because each $X(N\text{I}) = 1$ level will split into two closely spaced sets of three levels that are separated by approximately 6 GHz due to large $^{172}$Yb ($I = 5/2$) magnetic and nuclear electric quadrupole hyperfine interactions, similar to $^{172}$YbF [72].

In closely related work, [73] recently demonstrated $\sim 10 \times$ enhanced production of YbOH by exciting Yb atoms to the metastable $^3P_1$ state inside a buffer-gas cell, greatly enhancing the flux in a buffer-gas beam. By combining such an enhanced source with previously demonstrated laser slowing, magneto-optical trapping, and transfer to an ODT, we estimate that trapping of $\sim 10^5$ molecules in an eEDM experiment is feasible$^7$. This would lead to an eEDM sensitivity surpassing the current limit of $< 1.1 \times 10^{-29}$ e cm [7]. Additional technical improvements, such as beam focusing [74], transverse confinement [75], and `few photon' slowing methods [76, 77], could further increase the sensitivity.

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$^6$ We note that emission to higher bending modes, where allowed by symmetry (e.g. to the $\tilde{X}(12\Sigma^0\text{I})$ state), may also become relevant at this level.

$^7$ This estimate is based on previously reported efficiencies for slowing and trapping diatomic molecules from CBGBs [37, 39, 41].
