Improved x-ray detection and particle identification with avalanche photodiodes

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Avalanche photodiodes (APDs) are commonly used as detectors for low energy x-rays. In this work, we report on a fitting technique used to account for different detector responses resulting from photoabsorption in the various avalanche photodiode layers. The use of this technique results in an improvement of the energy resolution at 8.2 keV by up to a factor of 2 and corrects the timing information by up to 25 ns to account for space dependent electron drift time. In addition, this waveform analysis is used for particle identification, e.g., to distinguish between x-rays and MeV electrons in our experiment. © 2015 AIP Publishing LLC. [http://dx.doi.org/10.1063/1.4921195]

I. INTRODUCTION

Avalanche photodiodes (APDs) are silicon-based solid state detectors that convert photons into a charge current. They provide a compact, robust, magnetic field insensitive solution for light and x-ray detections with gains on the order of 100 and fast response times.¹–⁴ Due to this, APDs are extensively used in a large variety of physics,⁵–⁸ medical,⁹ and aerospace applications.¹⁰

We have studied x-rays with energies between 1 and 10 keV and observed two distinct APD responses to monoenergetic x-rays absorbed in different depths inside the APD. By constructing APD specific standard traces and using a pulse-by-pulse fitting technique, we improved the APD energy resolution by a factor of 2 and the time resolution by 30%. In addition, we were able to identify background signals stemming from electrons that deposit a few keV energy in the APD.

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The data presented in this work were gathered in the muonic helium Lamb shift experiment,¹¹,¹² using a set of twenty large area avalanche photodiodes (LAAPDs) from radiation monitoring devices (model S1315; 13.5 x 13.5 mm² active surface area each). The muonic helium ions represent an extended x-ray source that emits predominantly monoenergetic x-rays of 1.52 keV and 8.22 keV as well as electrons with up to 50 MeV of kinetic energy (see the Appendix). Previous tests of these APDs found 40% detection efficiency for 8.2 keV x-rays and an average energy resolution of 16% (FWHM) after calibration.¹³

Our x-ray detection setup consists of two linear arrays of 10 LAAPDs each, in which each LAAPD is mounted on a separate titanium piece for efficient cooling and easy replacement.¹³ The detector arrays are mounted inside a vacuum around 10⁻³ hPa and inside a 5 Tesla magnetic field, above and below the x-ray source. Custom-built low-noise, fast response preamplifiers are fitted to the LAAPDs. Both LAAPD/preamplifier assemblies are cooled using an external ethanol circulation system and are actively temperature stabilized at around −30 °C. The achieved short term temperature stability was better than ±0.1 °C. Highly stable temperatures are crucial for the operation of LAAPDs since their gain depends strongly...
on their operating temperature. Bias voltages were chosen to provide the best energy resolution per APD and ranged from 1.61 kV up to 1.69 kV, approximately 50 V below the breakdown voltage. The pre-amplifiers with two bipolar input transistors in cascode configuration (BFR 182 npn, BFT 92 pnp) have been used for the generation of a fast response from the large capacitance (120 pF) of the LAAPD. An overall gain of 150 mV/µA at 50 Ω has been measured with a test pulse. Outgoing APD signals were further amplified by gain 4 main-amplifiers and fed to the CAEN v1720 waveform digitizers (250 MS/s, 12 bit) for recording.

Our experiment requires pileup detection in the x-ray detectors to reduce background effects. Standard shaping amplifiers that are commonly used feature integration times too long to separate pulses on a 100 ns scale. This deteriorated the performance in our previous measurements where we used Rutherford Appleton Laboratory (RAL) 108A pre-amplifiers with µs-long integration times (see Ref. 13, Fig. 16). For our new project, we used fast pre-amplifiers with 30 ns rise time. When calculating a simple integral over the recorded pulses, a poor energy resolution became visible as seen in our previous measurement.

To compensate, we developed a simple standard response fitting technique that allowed us to distinguish between different responses on a hit-by-hit basis, improving the energy resolution by a factor of two (see Fig. 1, bottom) and correcting for a 25 ns time shift between both signal types as discussed in Sec. IV.

In Secs. II–VI, the different features of the measured x-ray signals are discussed before the fitting routine and the improved energy calibration are presented. Then timing difference between both responses and the influence of electron signals in the analysis are reviewed before a brief summary and outlook is given.

II. APD X-RAY RESPONSE

The working principle of the APDs used in our setup is explained in Fig. 3. In the conversion region (II), incoming photons produce primary photoelectrons. Differences in the thickness of this layer give rise to changes in detector energy acceptance. A p-n junction is placed on the back side of the active volume creating high local field strengths. Inside this avalanche region (III), electron impact ionization at the high field p-n+ junction leads to a multiplication of free charge carriers providing gain for the initially converted primary photoelectrons. The calculated absorption length for 8.2 keV and 1.5 keV x-rays is 70 µm and 9 µm, respectively. Due to the extended size of our x-ray source, the average incident angle of 52° in our geometry gives rise to an effective 1.6 times longer average path inside the APDs. This absorption length for 8 keV x-rays is similar to the APD layer thicknesses and therefore leads to a number of different effects on the APD output depending on the region where the photon is absorbed. The different possibilities are also shown and explained in Fig. 3.
III. X-RAY ENERGY DIFFERENCES AND COMPENSATION

In order to investigate this effect, a set of roughly $2.5 \times 10^4$ x-ray traces was recorded per APD. Fitted baseline fluctuations were below 10 mV for all analyzed signals, compared to average signal amplitudes of 500 mV for 8.2 keV x-rays. Our analysis routine starts with an edge finder (square weighting function with a width of 200 ns) to find the beginning of the pulse in the recorded trace. Then the slope of the leading edge is fitted with a linear function. Using a $\chi^2$ criterion, we improve the accuracy of the slope determination by varying start time of the pulse within 20 ns while keeping the fitting window fixed. Finally, we normalize the slope to the pulse integral provided by the edge finder to obtain the (amplitude-independent) rise time of the pulse.

When the rise time is plotted versus the integral of the pulse, four different contributions to the spectra can be identified as seen in Fig. 4. The two most prominent peaks are created by converted 8.2 keV photons with slow and fast detector responses, labeled slow 8 keV and fast 8 keV, respectively. For these peaks, we see a clear difference in rise time and integral while most of the low energy 1.5 keV x-rays show a slow rise time. The rise time distribution for small signals is broadened due to low amplitudes and noise.

The last visible component is generated by the already mentioned high energy (up to 50 MeV) electrons (created by muon-decay, further explained in the Appendix). These electrons deposit energies up to 50 keV in the APDs and their signals display a third kind of standard pulse shape, namely, a mixture of fast and slow x-ray pulse shapes. This is shown in the lower panel of Fig. 2.

In order to further analyze the two classes of 8.2 keV x-rays, two sets of APD traces for slow 8 keV and fast 8 keV were created by selecting the respective peaks in Fig. 4 with adequate cuts. A collection of selected traces for the slow 8 keV and fast 8 keV cases is shown in Fig. 2. For each of the two x-ray classes, traces were numerically averaged after shifting each trace to correct for the variation of the

![FIG. 3. Working principle of avalanche photodiodes based on a p+–i–p–n+ doping profile. The weakly doped intrinsic part (II) serves as conversion region for most incoming x-rays (case 1). Photoelectrons created are transferred towards the avalanche region. In this high field area, secondary electrons are generated through impact ionization providing charge gain. Low energy x-rays have a high probability of being stopped in the initial drift region (case II). These experience additional signal delay and reduced gain. Some photons convert in the multiplication region (III), also leading to reduced signal amplitudes (case 3). More about this effect can be found in Ref. 17. The bottom figure shows the electric field profile in the several regions of the APD together with the x-ray absorption profile for 1.5 keV and 8.2 keV x-rays.](image1)

![FIG. 4. Normalized slope of the rising edge plotted versus the integral of the pulse. The x-axis (color scale) is logarithmic. Integrals are roughly proportional to the deposited energy of the registered x-rays. Four contributions are visible: low energy 1.5 keV x-rays show integrals below 200. The recorded 8.2 keV x-rays create two different responses in the APD, one with slow rise time (slope $\approx 0.3$) and one with significantly faster rise time (slope $\approx 0.7$). The last contribution with an integral above 700 arises from MeV electrons depositing keV energy in the APD active region.](image2)
pulse starting time. This averaging created the standard traces of the subsets \( (T_{\text{slow}} \text{ and } T_{\text{fast}}) \). These traces had to be produced once per each APD for a measurement period of several months and stayed constant throughout multiple heating/cooling cycles of the APD assembly.

For the final analysis, each APD pulse is fitted with all available standard traces. Starting at the time provided by the edge finder, the standard trace is fitted to the pulse. The timing is then varied and the \( \chi^2 \) is recorded for each fit. To save computational effort that would arise for a 2-parameter fit (amplitude and time), the amplitude of the standard trace is always fixed by matching its integral to the integral of the signal (after baseline subtraction) in a 200 ns wide time window.

Finally, the minimal \( \chi^2 \) between the various standard traces is used to separate the pulses into different classes: slow 8 keV and fast 8 keV (and electrons, see below). The result from the best-fitting class is used to get amplitude, integral, and timing values of the recorded signal.

The allocation of the recorded APD signals in the slow 8 keV and fast 8 keV classes according to the fit routine can be seen in the top parts of Fig. 5. Calibration of the two x-ray spectra created by the \( T_{\text{slow}} \) and \( T_{\text{fast}} \) fits is done by matching the peaks in both separate integral spectra to the respective energy of 8.2 keV. As expected, the fast 8 keV component of x-rays is the largest part of the recorded signals in our setup as seen in Fig. 5. The observed 1:1.7 ratio of fast 8 keV to slow 8 keV x-rays agrees roughly with the expected absorption ratio of 1:1.5 estimated from the thicknesses of layers (I) and (II).

IV. X-RAY TIMING DIFFERENCES

In addition to the variation in the observed 8.2 keV x-ray energy, we were also able to measure a difference in timing between the fast 8 keV and the slow 8 keV components.

In order to achieve a common timing reference point for this study, coincidence events between the 8 keV x-rays recorded in the APD under investigation and the 1.5 keV x-rays registered in neighboring APDs were studied. These two x-ray types are emitted within a picosecond time window from the muonic atoms used (as is further explained in the Appendix).

Special attention was given to time calibration in order to avoid possible timing shifts created by the distinct standard traces \( T_{\text{fast}} \) and \( T_{\text{slow}} \) used for different signals. Therefore, calibration of the different APDs and traces against each other was done using the supplementary measured electron signals. The MeV electrons create hits in multiple detectors on their spiraling motion in the surrounding magnetic field enabling us to get a common timing for all APDs.

When comparing the timing of the measured 8.2 keV x-rays, we observed a 25 ns delay between slow 8 keV signals and normal fast 8 keV signals. A time spectrum showing this effect for a single APD is shown in Fig. 6. Correcting for this effect improves the APD time resolution of our setup by more than 30% when the two responses seen in Fig. 6 are unified. Better results might be achieved when a more clearly defined common timing is provided since the timing resolution is limited by the low amplitude 1.5 keV signals just above the noise level.

V. MeV ELECTRON DETECTION WITH APDS

Apart from the improved energy resolution that was achieved with the methods described in Sec. III, we were also able to differentiate high energy electron signals in the APDs from similar x-ray signals. These MeV electrons deposit

\[\text{Counts} \quad \begin{array}{c}
\text{Best Fit} \\
T_{\text{fast}} \\
T_{\text{slow}} \\
T_{\text{elec}} \\
\text{Sum}
\end{array} \]

\[\text{Energy [keV]} \]

\[\text{Counts} \quad \begin{array}{c}
\text{fast 8 keV} \\
\text{slow 8 keV}
\end{array} \]

\[\text{Time [ns]} \]

Fig. 5. Energy spectra of recorded x-rays and electrons in the muonic helium Lamb shift experiment categorized by the standard trace which provides the lowest \( \chi^2 \) in a range of 200 ns after the leading edge of the pulse. All spectra show two prominent peaks at 1.5 keV and 8.2 keV. The fast rising component provided by \( T_{\text{fast}} \) in dark blue enfolds signals converted in or behind the conversion region (II). It consists mostly out of 8.2 keV x-rays and the visible low energy tail is created by the loss of gain for x-rays converted in the avalanche region (III). The light blue distribution stands for all traces that were best described by the slow rising pulse shape \( T_{\text{slow}} \) and consists mostly out of 1.5 keV x-rays and some 8.2 keV x-rays mixed in. Signals best matching the electron trace \( T_{\text{elec}} \) are shown in the orange division. These signals are formed by a continuous electron background and a contribution of wrongly identified x-rays.

Fig. 6. Spectra showing the relative timing between slow 8 keV and fast 8 keV x-rays for a single APD. These time spectra have been obtained by plotting the time of the 8.2 keV x-ray signal detected in a LAAPD relative to the 1.5 keV signal detected in another LAAPD for both classes. Both LAAPDs including preamp-delay line, etc., have been synchronized using electrons. The origin is chosen as the center of gravity of the slow 8 keV response. A 25 ns timing difference could be measured between both responses. The relatively poor time resolution is given by the coincident 1.5 keV x-rays that are detected just above the noise level in our setup leading to a washed out signal.
up to 50 keV in the APD active volume and were always present in the experiment. Due to their passage through all the APD layers, electrons show signals with yet another shape that can be distinguished from the previously discussed fast and slow x-ray responses. A third standard trace $T_{\text{elec}}$ was created by averaging a set of clearly identified electron signals that correspond to a mean energy of 12 keV. This was done supplementary to the already known x-ray traces $T_{\text{slow}}$ and $T_{\text{fast}}$. A comparison of an electron induced signal shape at 8.2 keV and the respective real x-ray traces is also shown in Fig. 2 (bottom). As electrons with MeV energies deposit energy in all three APD layers (I, II, III), the corresponding standard trace $T_{\text{elec}}$ can be approximately parameterized as a mixture of the $T_{\text{slow}}$ and $T_{\text{fast}}$ standard responses. Using the same routine as for the previous pulse analysis, the tool was able to differentiate between x-ray and electron signals with very high fidelity, leading to a correct electron identification in 86% of the cases.

VI. SUMMARY

We have observed effects from the APD layer structure that lead to two distinct responses to X-rays in the 6-10 keV range. The individual signal types can be identified with high fidelity by examining the rising edge of the measured pulses. Correcting for this effect improves the energy resolution by up to a factor of 2 depending on the APD. Additionally, we were able to correct for timing differences between both responses. While the different rise time classes were observed in all 20 APDs under investigation, only 6 of them showed a resolved double-peak structure in the energy spectrum obtained by a simple integral.

Using the rise time analysis, it was also possible to filter MeV energy decay electrons. An electron-specific standard trace was clearly distinguishable from the two different kinds of x-ray signals recorded for 8.2 keV x-rays. A $\chi^2$ fit of the signal shape was used to exclude them from the x-ray data with an overall effectiveness of 86%, while only 14% of the 8 keV x-rays were wrongly identified as electrons. This leads to significant background reduction in the $\mu$He Lamb shift experiment.11,12

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APPENDIX: THE $\mu$HE LAMB SHIFT EXPERIMENT

The data presented in this work were acquired using muonic helium ions as x-ray source during the recent $\mu$He Lamb shift experiment.11,12 The experiment is performed at the high intensity proton accelerator facility at Paul Scherrer Institute in Switzerland. Its purpose was to measure the different 2S $\rightarrow$ 2P transitions in the $\mu^4$He + and $\mu^2$He + exotic ions via laser spectroscopy. The required information about its environment and working principle will be briefly sketched in this section.

The accelerator physics environment leads to stringent demands on stability and robustness of the APDs and the analysis routine employed that exceed common specifications. For example, the APD arrays used are placed inside a 5 T solenoidal magnet where they are mounted next to a low pressure helium gas target. Muonic ions are created in this 20 cm long gas volume operated at 2-4 hPa by low energy muons that are provided by the accelerator beam line. The dataset described in this work was obtained during the $\mu^4$He + measurement campaign in 2013 that offers multiple transitions in the low keV x-ray region. These consist of the $L_\alpha$, $L_\beta$, and $L_\gamma$ transitions at 1.52 keV, 2.05 keV, and 2.30 keV, respectively, as well as the $K_\alpha$, $K_\beta$, and $K_\gamma$ transitions at 8.22 keV, 9.74 keV, and 10.28 keV, emitted by the muonic helium ions during the so-called atomic cascade within a time frame of few ns total.12

The muons decay after an average lifetime of 2.2 $\mu$s into muon neutrino, electron antineutrino and “high energy” electrons in the MeV range. These electrons deposit energy when transversing the APD, creating electron hole pairs in all regions of the APD quasi-simultaneously. The induced signals correspond to virtual x-ray energies of up to 50 keV. This would raise background effects for the experiment that uses the recorded 8.2 keV $\mu^4$He + $K_\alpha$, x-rays as signal for laser spectroscopy. Therefore, a supplemental set of 4 plastic scintillators surrounds the gas target and APD arrays for additional means of electron detection and exclusion of background. Since the overall detection efficiency for electrons in the mentioned plastic scintillators is only roughly 30%, additional means for electron identification were desirable. This was achieved by waveform analysis described in Secs. III and V.

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