Star-Forming Galaxies at Cosmic Noon

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Abstract

Ever deeper and wider lookback surveys have led to a fairly robust outline of the cosmic star formation history, which culminated around $z \sim 2$ -- a period often nicknamed “cosmic noon.” Our knowledge about star-forming galaxies at these epochs has dramatically advanced from increasingly complete population censuses and detailed views of individual galaxies. We highlight some of the key observational insights that influenced our current understanding of galaxy evolution in the equilibrium growth picture:

• scaling relations between galaxy properties are fairly well established among massive galaxies at least out to $z \sim 2$, pointing to regulating mechanisms already acting on galaxy growth;
• resolved views reveal that gravitational instabilities and efficient secular processes within the gas- and baryon-rich galaxies at $z \sim 2$ play an important role in the early build-up of galactic structure;
• ever more sensitive observations of kinematics at $z \sim 2$ are probing the baryon and dark matter budget on galactic scales and the links between star-forming galaxies and their likely descendants;
• towards higher masses, massive bulges, dense cores, and powerful AGN and AGN-driven outflows are more prevalent and likely play a role in quenching star formation.

We outline emerging questions and exciting prospects for the next decade with upcoming instrumentation, including the James Webb Space Telescope and the next generation of Extremely Large Telescopes.


1. INTRODUCTION

1.1. Background

Star-forming galaxies at redshift \( z \sim 2 \), 10 billion years ago, trace the prime formation epoch of today’s massive disk and elliptical galaxies. Our knowledge about their properties, and their place in the global context of galaxy evolution, has undergone spectacular advances in the past two decades from both increasingly complete population censuses at ever earlier cosmic times and increasingly detailed descriptions of individual systems. The identification and characterization of galaxies according to their global colors, stellar populations, structure and morphologies, and environment is now routinely done out to \( z \sim 3 \), encompassing 85% of the Universe’s history. Comprehensive surveys of the kinematics and interstellar medium (ISM) properties have been obtained from spatially- and spectrally-resolved observations of ionized gas line emission out to \( z \sim 3 - 4 \). The cold gas content has been measured, and is being resolved on subgalactic scales for rapidly rising numbers. Growing samples at \( z \sim 4 - 8 \) are being assembled and the first candidates have been identified at \( z \sim 9 - 11 \) within 500 Myr of the Big Bang, yielding insights into the progenitor populations
of $z \sim 2$ star-forming galaxies.

This body of observational work has led to a fairly robust outline of the evolution of the stellar mass build-up and star formation activity of galaxies and the growth of supermassive black holes (SMBHs) over most of the Universe’s history (Madau & Dickinson 2014). As much as half of the stellar mass observed in galaxies today was formed in just about 3.5 Gyr between $z \sim 3$ and $z \sim 1$. After a rapid rise $\propto (1 + z)^{-2.9}$, the cosmic star formation rate (SFR) volume density peaked around $z \sim 2$ and subsequently declined as $\propto (1 + z)^{2.7}$ to $z = 0$. The comoving rate of SMBH accretion follows a similar evolution, in support of co-evolution of central black holes and their host galaxies. This evolution in cosmically averaged rates finds its counterpart in the observed properties of individual star-forming galaxies (SFGs), which around $z \sim 2$ were forming stars and feeding their central black holes $\sim 10$ times faster than today’s SFGs. At least up to $z \sim 3$, the vast majority of SFGs follows tightly a roughly linear “main sequence” (MS) between SFR and stellar mass (e.g., Rodighiero et al. 2011, Speagle et al. 2014), whose zero-point evolution reflects the decline in cosmic SFR density to the present time. Other scaling relations involving size, kinematics, metal, and gas content are also observed as early as $z \sim 2−3$ (e.g., van der Wel et al. 2014a, Ubler et al. 2017, Maiolino & Mannucci 2019, Tacconi et al. 2020). Detailed mapping of the distribution and motions of stars and gas within galaxies have begun to probe the internal workings of galaxy evolution, and the spatial and temporal progression of the build-up of galactic components. Despite increasingly clumpy and irregular appearances at higher redshift, more so in the rest-frame ultraviolet (e.g., Conselice 2014), there is now compelling evidence that the bulk of (massive) SFGs have global disk-like stellar light distributions and kinematics (e.g., Wuyts et al. 2011b, Wisnioski et al. 2019).

1.2. Setting the Stage

Once dubbed the “redshift desert” because of the relative inaccessibility of key spectral features for source identification with then available instrumentation, our matured view driven by rapid observational progress now shows that $z \sim 1−3$ is a pivotal epoch in galaxy evolution — it is “cosmic noon”.

Lookback studies are at a turning point, with major leaps forward anticipated in the next decade from cutting-edge instrumentation at existing observatories, the imminent launch of the James Webb Space Telescope (JWST), and the coming of next-generation large aperture ground-based telescopes such as the 39 m Extremely Large Telescope (ELT), the Thirty Meter Telescope (TMT), and the 25 m Giant Magellan Telescope (GMT). Recent and future capabilities at current facilities will allow us to establish the missing links between
the distributions and kinematics of stars, gas, and metals in and around galaxies, unraveling vital phases of the baryon cycle and the interplay between baryons and dark matter. With transformative boosts in sensitivity and angular resolution afforded by JWST and the extremely large telescopes, galaxy evolution at \( z > 1 \) will be charted with unprecedented completeness well into the epoch of reionization and with unrivaled sharpness down to the 100-pc scale of individual giant star-forming complexes — a landscape revolution akin to the advent of the Hubble Space Telescope (HST) and the first 8 m-class telescopes in the 1990s.

Of the remarkably rich observational harvest of the past 5-10 years, we can here only highlight select aspects that have been among the most influential in advancing our knowledge about \( z \sim 2 \) SFGs. We focus on the internal properties of galaxies as revealed by diagnostics in emission and typical environments found in deep extragalactic fields, which comprise the bulk of the galaxy population. Section 2 presents the observational landscape. Section 3 discusses global properties providing the population context and enabling evolutionary links, and Section 4 zooms on resolved properties providing insights into the physics shaping galaxies. Section 5 discusses subpopulations of SFGs with extreme properties. Section 6 briefly comments on the theoretical landscape. In closing, Section 7 summarizes the article, and outlines open issues and future observational opportunities.

For simplicity, we refer throughout to the \( 1 \lesssim z \lesssim 3 \) epochs as “\( z \sim 2 \)” or “high \( z \)” unless explicitly stated otherwise. We adopt a \( \Lambda \)-dominated cosmology with \( H_0 = 70 \text{ km s}^{-1} \text{ Mpc}^{-1} \), \( \Omega_m = 0.3 \), and \( \Omega_\Lambda = 0.7 \). For this cosmology, \( 1'' \) corresponds to 8.4 kpc at \( z = 2 \). Magnitudes are given in the AB photometric system. Where relevant, galaxy masses and star formation properties are adjusted to a common Chabrier (2003) stellar initial mass function (IMF).

2. OBSERVATIONAL LANDSCAPE

The dramatic advances in our knowledge about galaxies at cosmic noon have been driven by the confluence of novel observational techniques and sensitive high-multiplex ground- and space-based instrumentation across the electromagnetic spectrum. The concentration of multi-wavelength campaigns in select fields targeted as part of the Great Observatories Origins Deep Survey (GOODS), the Cosmic Evolution Survey (COSMOS), the All-wavelength Extended Groth strip International Survey (AEGIS), and the UKIDSS Ultra-Deep Survey (UDS) have yielded rich data sets and have seen their legacy value fully realized by providing samples of choice for many detailed follow-up studies. Several reviews have covered various aspects of \( z > 1 \) galaxy surveys in the past decade (notably Shapley 2011, Glazebrook 2013, Madau & Dickinson 2014, Lutz 2014, Conselice 2014, Tacconi et al. 2020). This Section gives an update incorporating recent programs with the goal of highlighting the observational underpinnings of our current physical understanding of cosmic noon galaxies.

Our empirical knowledge rests on a ladder going from the identification of galaxies from large photometric samples and their spectroscopic confirmation enabling statistical descriptions of the population, to increasingly detailed studies of subsets from spectrally/spatially resolved data. Observations at optical to near-IR wavelengths form a major part of each step, probing the redshifted, rest-frame UV to optical emission from \( z \sim 2 \) galaxies. Figure 1 identifies salient spectral features on a model spectrum created for an example SFG at \( z = 2.3 \) and shows how they shift across the various atmospheric bandpasses from \( z = 1 \) to 3. These features include (with rest wavelengths given in Å):

- hydrogen recombination and atomic forbidden emission lines from warm ionized gas
excited by star formation, AGN, and shock activity, which provide diagnostics of nebular conditions, dust attenuation, galaxy dynamics, and gas outflows (Lyαλ1216, Hβλ4861, Hαλ6563, [OII]λλ3726,3729, [OIII]λλ4959,5007, [SII]λλ6716,6730);

- stellar continuum emission, encompassing the Balmer discontinuity at 3646Å and the 4000Å break caused by hydrogen and multiple metallic species and molecules in the atmospheres of intermediate- to low-mass evolved stars, and on which estimates of the stellar age, stellar mass, and dust reddening are based;

- a rich suite of far-UV (≈ 1200 – 2000Å) interstellar low- and high-ionization atomic absorption lines useful to trace gas outflows/inflows, alongside various other absorption and emission features from stellar photospheres and winds, and gas photoionized by hot stars and AGN (including SiIIλ1260, the blend OI+SiIIλ1303, SiIIλ1334, SiIVλλ1393,1402, CIVλλ1548,1550, FeIIλ1608, AlIIλ1670);

- weaker but important interstellar MgIIλλ2796,2803 absorption (another common ISM and outflow diagnostic) and the faint auroral [OIII]λ4363 line (a temperature-sensitive indicator in direct-method gas metallicity estimates).

Figure 2 illustrates the ladder of surveys in terms of spectral resolution vs. the number of galaxies within the 1 < z < 3 interval of interest for this article. The full list of surveys and main references are compiled in the Supplemental Tables 1 and 2.

2.1. Photometric Surveys in the Optical to Near- /Mid-infrared

Imaging in multiple photometric bandpasses is the most efficient way to identify and characterize large numbers of galaxies over a wide redshift range. Imaging campaigns at optical to mid-IR wavelengths (λobs ~ 0.3 – 8 μm) with sensitive cameras at ground-based telescopes and from space with HST and the Spitzer Space Telescope (hereafter Spitzer) have provided...
Overview of selected optical/near-IR surveys covering $1 < z < 3$ as a function of number of sources in this interval and spectral resolution (see list in Supplemental Tables 1 and 2). The color-coding indicates the primary type of observations: photometric imaging (light grey); photometric imaging including high-resolution HST data (blue) and subsets thereof with useful (i.e., S/N $> 3$) medium-/narrow-band data (dark blue); slitless grism data from HST (cyan); optical spectroscopy (green); near-IR spectroscopy (yellow); near-IR IFU data (red; detailed in Figure 3). Different symbols distinguish surveys of gravitationally lensed targets and/or areas (diamonds) from unlensed ones (circles); for the HFF, the full survey (including parallels) and subsets magnified by $\mu > 2$ and $\mu > 10$ are plotted. The inset shows the combined redshift distributions, grouped and color-coded by observations type, normalized by the total number of $1 < z < 3$ galaxies, and with fractions on a logarithmic scale. Given the very heterogeneous nature of the samples (depth, detection/selection function, etc.), the histograms merely serve to illustrate the typical relative distributions. The overall drop with increasing $z$, smoothest for photometric and grism surveys, largely reflects the flux limits; the turn-up at $z \sim 3$ for photometric-only surveys is driven by efficient Lyman-break dropout identification in optical surveys. Key spectral features falling between atmospheric windows cause the $z$ gaps for ground-based spectroscopic and IFU surveys.

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**SED**: Spectral energy distribution.

**$z_{\text{phot}}$**: Photometric redshift, based on the broad/medium/narrow-band SED.

**$R = \lambda/\Delta \lambda$**: Spectral resolution given as the ratio of wavelength to the full-width at half-maximum of a filter bandpass or spectral line spread function.

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the most extensive censuses of distant galaxies. At $z \sim 2$, the multi-color information is primarily sensitive to the shape of the stellar continuum modulated by interstellar dust. The spectral energy distribution (SED) of galaxies is used to derive photometric redshifts ($z_{\text{phot}}$) and basic properties such as stellar mass and SFR (for techniques, see Salvato et al. 2019 and Conroy 2013, respectively, and Supplemental Text).

The inclusion of near/mid-IR wavelengths has been crucial to the inventory of the full population by detecting red optically-faint galaxies, probing wavelengths where outshining by young hot stars and attenuation by dust are reduced, and allowing to better trace the light from cooler stars that dominate the stellar mass. At $z \sim 2$, near-IR data are particularly important to gain leverage from the fairly sharp Balmer/4000 Å continuum breaks. Photometry in broad bandpasses is most sensitive but delivers coarse spectral resolution with typically $R = \lambda/\Delta \lambda \sim 5 - 10$. The addition of medium-band ($R \sim 10 - 20$) and narrow-band ($R$ up to $\sim 100$) information has proven vital to improve the accuracy and reliability of photometric redshifts and galaxy parameters (e.g., Ilbert et al. 2009, Whitaker 2009).
least two spectral features of the data, the wavelength range probed, and the galaxy type. For instance, it is easier and/or from stellar absorption features. To be secure, \( z \) is adequate to measure redshifts to within \( \sim R > 300 \) km s\(^{-1} \) or better from ISM emission lines and/or from stellar absorption features. To be secure, \( z \) ’s rely on the identification of at least two spectral features\(^1\) and the success also depends on the signal-to-noise ratio (S/N) of the data, the wavelength range probed, and the galaxy type. For instance, it is easier to

\[ L^* : \text{characteristic value of the galaxy luminosity distribution described by a Schechter function:} \]

\[ \Phi(L) \approx (\phi^*/L^*) \times (L/L^*)^\alpha e^{-L/L^*} \]

See Marchesini et al. (2012) and Parsa et al. (2016) for rest-optical and UV luminosity functions out to cosmic noon.

\[ z_{\text{spec}} : \text{Spectroscopic redshift, based on a spectrum (typically at} \ R > 200) \]

\[ S/N : \text{Signal-to-noise ratio.} \]

\(^1\) A distinct profile such as the characteristic asymmetry of Ly\( \alpha \) or doublets such as [OII] \( \lambda 3726,3729 \) can be sufficient if these lines are observed.

2.2. Spectroscopic Surveys in the Optical to Near-infrared

Spectroscopic redshifts (\( z_{\text{spec}} \)) are essential to validate and optimize \( z_{\text{phot}} \) techniques, construct the most precise galaxy distribution functions from confirmed samples, and provide secure targets for detailed and time-consuming follow-ups. Spectroscopy at \( R > 200 \) is adequate to measure redshifts to within \( \sim 300 \) km s\(^{-1} \) or better from ISM emission lines and/or from stellar absorption features. To be secure, \( z_{\text{spec}} \)’s rely on the identification of at least two spectral features\(^1\) and the success also depends on the signal-to-noise ratio (S/N) of the data, the wavelength range probed, and the galaxy type. For instance, it is easier to
measure the redshift of a source with higher emission line or continuum surface brightness, introducing a notorious bias towards bluer, more compact, more star-forming galaxies at $z > 1.5$ in optical spectroscopic surveys. The challenges of confirming large samples at $z \sim 2$ are manifold. The galaxies are faint. At $z = 2$, $L_{UV}$ corresponds to $R \sim 24.5$ mag and $L_V$ to $H \sim 22.3$ mag, often necessitating long integrations to reach a sufficient S/N for $z_{\text{spec}}$ measurements even with 8 m-class telescopes. Absorption and emission features observable in the optical are typically weak. The stronger nebular emission lines are shifted into the near-IR regime that is plagued by a dense forest of $>1000$ bright and variable emission lines mostly from OH radicals excited in the upper atmosphere, broad intervals of low atmospheric transmission around 1.4 and 1.9 $\mu$m, and thermal background from instrument to infrastructure and atmosphere at $\lambda_{\text{obs}} > 2$ $\mu$m.

In the optical, great progress has come from high throughput multi-object spectrographs (MOS) such as Keck/LRIS and DEIMOS and VLT/VIMOS and FORS2, optimized to extend bluewards to the atmospheric cutoff near 3000 Å or redwards to $\sim 1$ $\mu$m to overcome the “redshift desert.” The more recent arrival of sensitive cryogenic near-IR MOS, including Keck/MOSFIRE and Subaru/FMOS and MOIRCS, further expanded confirmed $z \sim 2$ samples mainly through rest-optical emission lines. Near-IR observations from space have an obvious advantage and use of the HST/WFC3 grism G141 with $R \sim 130$ has been very productive at yielding redshifts. The lack of atmosphere ensures continuous coverage of the full $\lambda_{\text{obs}} = 1.1 - 1.7$ $\mu$m grism window and greatly enhances continuum sensitivity, reducing biases towards line-emitting sources. The slitless aperture maximizes multiplexing and avoids target pre-selection biases, with the added ability to map spectral features at HST’s angular resolution. Reliable grism redshifts ($z_{\text{grism}}$) from the 3D-HST and AGHAST programs [Momcheva et al. 2016], for instance, have nearly tripled the number of $1 < z < 3$ galaxies with secure spectroscopic redshifts in the five CANDELS fields, with typical $z_{\text{grism}}$ accuracy of $0.003 \times (1 + z)$ ($\sim 1000$ km s$^{-1}$ at $z \sim 2$) at $JH \leq 24$ mag, and only 2–3× worse for the subset of quiescent galaxies.

Besides redshift, spectra also provide a wealth of information on the stellar, gas, dust, and AGN content of galaxies. Detailed information is more demanding in terms of S/N and spectral resolution, to measure accurate emission and absorption line strengths and profiles for a range of fluxes and equivalent widths, and to deblend spectral features (e.g., [OII] and [SII] doublets, or kinematic components such as host disk and gas outflow). Among many results from MOS surveys at $z \sim 2$, scaling relations have been constructed such as the MS using SFR estimates from Balmer lines or UV luminosities, and the mass-metallicity(-SFR) relationship from strong line diagnostics of the gas-phase oxygen abundance. Excitation sequences in nebular line ratio diagrams have been examined to characterize the evolving ISM conditions at high $z$. Galaxy kinematics have been investigated from integrated line widths and, with data subsets of sufficient spatial resolution and suitable slit alignment, from velocity gradients. The demographics and energetics of galactic outflows have been investigated from the strength and velocity profile of rest-UV interstellar absorption and rest-optical nebular line emission. In addition, stellar and dynamical properties of smaller but important samples of massive quiescent galaxies have been constrained from absorption (and in some cases weak emission) features – valuable to establish the fate of massive SFGs from their likely immediate descendants. These results are discussed throughout Sections 3, 4 and 5.

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**MOS**: Multi-object spectroscopy, or spectrograph.

**VLT**: Very Large Telescope.

**$z_{\text{grism}}$**: Redshift from grism spectroscopy, here specifically from HST $R \sim 130$ grism data supplemented with photometric SEDs.
2.3. Integral Field Spectroscopic Surveys

Imaging spectroscopy at $R \gtrsim 2000$ arguably provides the richest datasets of individual sources — a large multiplexing of its own. Integral field unit (IFU) spectroscopy is the most efficient technique — collecting simultaneously the full three-dimensional (3D) spatial and spectral information — and became possible for $z \sim 2$ SFGs (with typical Hα fluxes of $\sim 10^{-16}$ erg s$^{-1}$ cm$^{-2}$ or fainter) with sensitive near-IR IFU instruments at 8 m-class telescopes. IFU studies have so far mainly used Hα+[NII] line emission (or [OIII]+Hβ at $z \geq 2.7$) to map the internal gas motions of galaxies, the distribution of star formation, gas excitation, and ISM metallicities within them, and the extent and properties of the gaseous winds they expel. Key results on these topics are covered in Sections 3 and 4.

First samples were obtained with single-IFUs including VLT/SINFONI, Keck/OSIRIS, and Gemini/NIFS, all with resolving powers of $R \sim 2000 - 5000$ and designed to be fed by an adaptive optics (AO) system improving the angular resolution from typical near-IR seeing of $\sim 0.5 - 0.7$ at their sites to the diffraction limit of their host telescopes ($\sim 50 - 60$ mas at $\lambda_{\text{obs}} = 2 \mu$m). To date, near-IR single-IFU samples amount to $\sim 400$ targets altogether, with roughly half of these sources observed in AO mode. These samples, all drawn from spectroscopically-confirmed subsets of parent photometric samples with diverse primary selection criteria (magnitudes, colors, narrow-band identification, strong lensing) form a heterogeneous collection probing different parts in $z - M_\star - \text{SFR}$ space (e.g., Glazebrook 2013 Förster Schreiber et al. 2018 and references therein). Larger and more complete surveys have been enabled with the advent in 2013 of KMOS at the VLT, with 24 IFUs deployable over a 7′-diameter patrol field. KMOS operates in natural seeing, covers $0.8 - 2.4$ µm with four bandpasses at $R \sim 4000$ each, and is well suited to detect faint, extended line emission over a wide redshift span. With $> 2000$ SFGs targeted so far, KMOS has put results from single-IFU work on a more robust statistical footing (e.g., Wisnioski et al. 2015, 2019, Harrison et al. 2016, 2017). Importantly, it has also allowed to push into regimes previously unexplored with IFUs, including line emission of massive sub-MS galaxies (Belli et al. 2017b), and continuum for stellar populations and kinematics of massive quiescent field and cluster galaxies (e.g., Mendel et al. 2015, Beifiori et al. 2017).

Figure 3 illustrates the observational and galaxy parameter space of the main near-IR IFU surveys of rest-optical line emission. The $\log(M_\star/M_\odot) \gtrsim 9.5$ SFG population is extensively covered; detections also extend to SFRs $\sim 10 \times$ or more below the MS, and to $\log(M_\star/M_\odot) \lesssim 9$ preferentially above the MS. While optical IFU spectroscopy is more relevant to $z \lesssim 1$ studies, synergies are increasingly exploited by combining near-IR IFU samples with recent optical wide-field IFU surveys with VLT/MUSE at intermediate redshifts and large $z \lesssim 0.15$ samples such as SAMI, CALIFA, and MaNGA observed with panoramic IFUs. Together, these surveys enable consistent comparisons and evolutionary links based on fully resolved kinematic and emission line properties from the same diagnostics over the past 11 Gyr of cosmic time.

2.4. Other Wavelengths as Probes of total SFRs, Cold Gas, and AGN

2.4.1. Infrared observations. Space-borne mid- to far-IR photometry with Spitzer/MIPS (at 24, 70, 160 µm) and then with Herschel (with PACS at 70, 100, 160µm and SPIRE at 250, 350, 500 µm) revolutionized IR surveys of distant galaxies thanks to their much improved sensitivity, angular resolution, and mapping speed compared to previous missions. They opened the window to statistical censuses of the dust-obscured component of the stel-
Figure 3
Overview of near-IR IFU surveys of line emission of $z \sim 1 - 3$ galaxies in observational and galaxy parameter space (see list in Supplemental Table 2). Left: The surveys are represented in terms of the average number of spectral bands covered per target, median on-source integration time per band (on a logarithmic scale), and number of objects targeted (with symbol area proportional to this number). Samples of field galaxies observed in natural seeing or with AO, and lensed galaxies in either mode, are plotted as circles, squares, and diamonds, respectively. The color coding denotes the median redshift of the samples. Right: Distribution of detected targets in stellar mass vs. MS offset for samples where these properties are available. Different colors and symbols are used to show the redshift, and differentiate field vs. lensed galaxies, and no-AO vs. AO data, as labeled in the plot. The underlying distribution of galaxies in a similar $z$ range to $H_{160} = 26.5$ mag from the 3D-HST catalog is shown in greyscale for comparison. The histograms compare the projected distributions in $M_\star$ of field galaxies observed in natural seeing (scaled by $\times 1/7$, in purple), field galaxies observed with AO (green), and lensed galaxies (yellow).

Spitzer/MIPS has delivered the deepest views of the dusty ISM of cosmic noon galaxies through 24 $\mu$m observations, enabling the detection of individual galaxies at $z \sim 2$ down to SFR $\sim 10 M_\odot$ yr$^{-1}$ (e.g., Whitaker et al. 2014). At these redshifts, however, 24 $\mu$m data measures rest-frame 8 $\mu$m light, where warm and transiently heated dust in HII regions and around AGN, polycyclic aromatic hydrocarbons arising from photodissociation regions, and absorption by silicate dust contribute. The conversion to total IR luminosity and SFR is thus prone to important uncertainties from the SED that needs to be assumed for the large extrapolation over the far-IR dust emission peak typically around rest-frame 100 $\mu$m (corresponding to a characteristic dust temperature of $\sim 30$ K). Measurements with submm instruments (e.g., JCMT/SCUBA and APEX/LABOCA) provided useful constraints on the Rayleigh-Jeans side, where AGN heating is minimized. The wavelength coverage and sensitivity afforded by Herschel has been vital in sampling directly the far-IR SED peak, enabling robust calorimetric estimates of galaxy SFRs (and cold dust properties).

2.4.2. Submm to mm observations. Observations in the submm to mm regimes probe the cold ISM component in galaxies. Its main constituent, $H_2$, lacks a permanent electric dipole moment hence relevant emission lines at low excitation temperatures. Therefore, the strong
rotational lines of CO (the second most abundant molecule) are used to trace molecular gas properties and kinematics of galaxies, with mid-\(J\) transitions (2-1, 3-2, 4-3) being commonly employed at \(z \sim 2\). Molecular gas masses (hereafter simply \(M_{\text{gas}}\)) are estimated via an excitation correction to the ground-state 1-0 line and a conversion from CO line luminosity to \(H_2\) mass (e.g., Bolatto et al. 2013; Genzel et al. 2015). The CO 1-0 transition is typically fainter than mid-\(J\) lines and is shifted into the high-frequency radio bands, accessible for instance with the JVLA. The cold dust continuum luminosity is a viable and observationally efficient proxy for the gas mass and spatial distribution (e.g., Scoville et al. 2017; Tacconi et al. 2018).

Great strides in cold ISM studies of \(z > 1\) galaxies have been made possible with the IRAM/NOEMA interferometer in the northern hemisphere and ALMA in the south. With the gains in sensitivity and angular resolution of these arrays, studies of the global cold ISM content have shifted from the most luminous “submm galaxies” to the more typical MS population, although substantial integration times are still needed especially for CO line measurements and the limited primary beam sizes hamper mapping of sizeable areas (see recent reviews by Combes 2018; Tacconi et al. 2020). Pointed CO or continuum surveys have been most efficient at assembling sets of \(\sim 10 - 100\) at \(z \sim 2\) drawn from well-characterized parent samples. Blank field mosaicking surveys have been undertaken to build censuses out to \(z \sim 4\), either optimized for emission line searches through spectral scans or emphasizing dust continuum emission, yielding so far a few to several 10’s of secure detections and with counterparts in the (deep) optical to mid-IR imaging available in the survey fields. Most of the CO and dust continuum measurements at \(z \sim 2\) are for massive \(\log(M_*/M_\odot) \gtrsim 10 - 10.5\) SFGs. Detection in less massive (unlensed) galaxies becomes increasingly difficult as the amount of gas gets lower, and the ISM metallicity drops leading to more extensive UV photodissociation of CO and lower dust abundances. Alternative cold ISM tracers in emission are not practical because of their weakness, or because their higher frequency make them difficult or impossible to access from the ground at these redshifts. An obvious avenue for the future, in reach of NOEMA and ALMA, is more systematic spatially-resolved sub-arcsec CO and dust mapping at \(z \sim 2\), which is currently limited to fairly small heterogeneous sets dominated by very luminous or massive galaxies (e.g., Tacconi et al. 2013; Silverman et al. 2015; Barro et al. 2017b; Tadaki et al. 2017a,b).

2.4.3. Radio observations. At longer radio wavelengths, continuum observations probe AGN and star-forming systems mainly through non-thermal synchrotron emission, free from dust/gas obscuration. In SFGs, the synchrotron emission is produced in supernova remnants and, towards higher frequencies, free-free emission from HH regions also contributes (Condon 1992). In AGN sources, the origin is more diverse, including jets, hotspots, and large-scale lobes, which complicates the quantitative relationship between observed radio emission and AGN luminosity (e.g., Tadhunter 2016). Surveys at 1.4 – 5 GHz and lower frequencies down to \(\sim 200\) MHz (\(\lambda \sim 6 - 150\) cm) with facilities such as the JVLA, VLBA, LOFAR, GMRT,GBT, and ATCA have been carried out in many cosmological deep fields, with a range of sensitivities, beam size, and area. AGN dominate at brighter flux densities while SFGs become increasingly important at sub-mJy levels. Given that the tight radio-IR luminosity correlation for SFGs holds out to at least \(z \sim 3\), with fairly well constrained (mild) evolution \((L_{\text{IR}}/L_{1.4\text{GHz}} \propto (1 + z)^\alpha)\), and \(\alpha\) in the range \(-0.1\) to \(-0.2\), the radio flux density can serve as SFR estimator, and the radio excess above the correlation can be used as diagnostic for the presence of an AGN (e.g., Magnelli et al. 2015; Delhaize et al. 2017). The deepest GHz-regime VLA imaging at \(\sim 1''\) resolution (in AEGIS, GOODS-N, COS-
2.4.4. X-ray observations. At the other end of the spectrum, observations of X-ray radiation (0.5 – 100 keV) in galaxies trace predominantly nuclear activity (e.g., [Brandt & Alexander 2015]). Produced in the immediate vicinity of the SMBH via Compton up-scattering in the accretion-disk corona, in powerful nuclear jets, and via Compton reflection and scattering interaction processes with matter throughout the nuclear regions, X-rays are able to penetrate through substantial gas columns (becoming hindered in the highly Compton-thick regime with \( N_{\text{H}} \gg 1.5 \times 10^{24} \text{ cm}^{-2} \)). Non-AGN X-ray emission in galaxies arises from X-ray binaries and hot gas but is both less energetic and softer compared to that of (luminous) AGNs. The most extensive cosmological surveys have been carried out with the spaceborne Chandra and XMM-Newton Observatories, operating since 20 years, with on-board instruments enabling efficient spectroscopic imaging of wide areas in soft and hard bands (\( \sim 0.2 – 2 \) and \( 2 – 10 \) keV), while the more recently launched NuSTAR telescope has started to unveil the distant universe in \( > 10 \) keV radiation. The deepest and sharpest views were achieved with Chandra/ACIS through the cumulative 7 Ms exposure of \( \sim 485 \) arcmin\(^2\) in the Chandra Deep Field-South (encompassing GOODS-S), yielding nearly 1000 detections to \( z \sim 4.5 \). While AGN dominate the source counts, the more so at higher \( z \) and luminosities, the depth of the data reaches intrinsic rest-frame \( 0.5 – 7 \) keV \( \log(L_{\text{X}}/\text{erg s}^{-1}) \lesssim 42.5 \) out to \( z \sim 3 \) ([Luo et al. 2017]), where SFRs from several 100 to 1000 \( M_{\odot} \text{ yr}^{-1} \) can be detected. Because the rapid variability of AGN emission at these energies and the potential presence of high absorbing gas columns near the nucleus can bias X-ray samples, AGN identification benefits from complementary diagnostics such as high-excitation rest-UV/optical emission lines, radio luminosity, and mid-IR colors (e.g., [Padovani et al. 2017]).

2.5. Mass-matching vs. Abundance-matching

In order to bring theoretical models and observations into the same arena for an apples-to-apples comparison, a common interface needs to be found. Different approaches can be employed, bringing this interface either very close to the direct observables (e.g., by treating numerical simulations with radiative transfer and/or placing them into a lightcone to predict number counts as a function of observed flux) or alternatively working from the observables backward to interpret them in terms of physical quantities (e.g., using the spectral modeling techniques outlined in the Supplemental Text). Once stellar population properties such as stellar masses are inferred from the multi-wavelength SEDs, and provided sufficient depth, mass-complete samples of galaxies can be extracted from the flux-limited parent catalog. Those in turn can serve as basis for population-averaged comparisons to models, where for example the evolution of the SFR, size, metallicity, rotational velocity or other physical quantity is traced as a function of redshift at fixed stellar mass. How far back the population-averaged evolution can be recovered depends on the mass regime considered, as the parent catalog’s flux limit will necessarily impose a redshift-dependent mass completeness limit.

While valuable, such population censuses do not by themselves reflect the growth histories of individual systems. Galaxies gain stellar mass through star formation and merging activity, moving out of the considered mass bin while others move in. Methods to empirically reconstruct evolutionary sequences for individual galaxies from the mass-complete
samples, linking their progenitor and descendant phases, gained significant attention in recent years. The most common ansatz is to assume the preservation of mass ranking, in which case progenitors and descendants are anticipated to live at the same comoving number density ([van Dokkum et al. 2010](#vanDokkum2010)). The resulting evolutionary tracks can then directly be compared to the main progenitor branch extracted from a galaxy formation model.

The efficacy of this technique relies in part on the infrequent occurrence of major galaxy mergers, and indeed refinements have been proposed on the basis of cosmological simulations to account for a non-negligible divergence in growth rates, in part influenced by merging activity ([van de Voort 2016](#vanDeVoort2016) [Wellons & Torrey 2017](#Wellons2017) [Clauwens et al. 2017](#Clauwens2017)). Here, it is of note that slightly different prescriptions are desired for tracing galaxies backwards vs. forward ([Torrey et al. 2017](#Torrey2017) [Wellons & Torrey 2017](#Wellons2017)), and that the technique is designed primarily to work when the galaxy population is well described as a one-parameter family characterized by stellar mass. If considering subpopulations defined by, e.g., mass and color, galaxies may not only enter a particular mass bin due to their stellar growth, but also their color evolution, potentially introducing progenitor bias (e.g., [Carollo et al. 2013](#Carollo2013)). Finally, from the perspective of the flux-limited parent catalog, the abundance matching technique leaves more of the collected data unused, as higher mass cuts are adopted at later times to identify progenitors and descendants, whereas the deepest mass completeness limits are reached at the lowest redshifts.

### STELLAR, GAS, AND STRUCTURAL PROPERTIES

- **$M_\star$, $M_{\text{gas}}$, $M_{\text{bar}}$**: Total stellar, cold molecular gas, and baryonic (stellar+gas) masses.
- **Schechter function**: Parametrization of the galaxy number density vs. stellar mass (or luminosity), with $\Phi(M) = (\phi_*/M_*) (M/M_*)^\alpha e^{-M/M_*}$ or $[(\phi_*/M_*) (M/M_*)^\alpha_1 + (\phi_*/M_*) (M/M_*)^\alpha_2] e^{-M/M_*}$ (single- or double-Schechter); the characteristic value $M_*$ is referred to as the Schechter mass ([Schechter 1976](#Schechter1976)).
- **sSFR**: Specific star formation rate, SFR/$M_\star$.
- **$\Delta M_S$**: Logarithmic offset in sSFR (or SFR) from the MS, log(sSFR/sSFR$_{\text{MS}}(M_\star, z)$).
- **SFH**: Star formation history; common forms include an exponential $\propto e^{-t/\tau}$, delayed $\propto te^{-t/\tau}$, or log-normal $\propto (t\sqrt{2\pi \tau^2})^{-1} e^{-0.5(ln(t)-t_0)^2/\tau^2}$ SFR where $t$, $\tau$, and $t_0$ are the time, timescale, and logarithmic delay time.
- **$n$**: Number density parameter of the double-Schechter.
- **$\Sigma_1$, $\Sigma_{\text{gas}}$, $\Sigma_{\text{SFR}}$**: Stellar mass, gas mass, and SFR surface densities conventionally within $R_e$, taking half the total light ($R_e$) and gas depletion time via star formation $\tau_{\text{depl}}$. Gas-to-baryonic mass fraction $M_{\text{gas}}/M_{\text{bar}}$, and gas depletion time via star formation $M_{\text{gas}}$/SFR.

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**Notes**

- **$M_\star$**: Total stellar mass.
- **$M_{\text{gas}}$**: Cold molecular gas mass.
- **$M_{\text{bar}}$**: Baryonic mass.
- **$\phi_*/M_*$**: Normalization parameter.
- **$\alpha$, $\alpha_1$, $\alpha_2$**: Slope parameters.
- **$\phi_*$**: Normalization parameter.
- **$M_*$**: Characteristic mass.
- **$\tau$**: Timescale.
- **$t_0$**: Logarithmic delay time.
- **$R_e$**: Effective radius, enclosing half the total light (or mass).
- **$R_d$**: Disk scalelength for an exponential profile $\Sigma(r) = \Sigma(0) \exp(-r/R_d)$, in which case $R_e = 1.68 R_d$.
- **$b/a$**: Projected minor-to-major axis ratio of an inclined disk (also denoted $q$).
- **$R_e^{\text{circ}}$**: Circularized effective radius, scaling $R_e$ by $\sqrt{b/a}$.
- **$R_0$**: Radius enclosing 80% of the total light (or mass).
- **$\Sigma_1$, $\Sigma_{\text{gas}}$, $\Sigma_{\text{SFR}}$**: Stellar, gas, and SFR surface density within the central 1 kpc, $M_\star(< 1\text{kpc})/\pi(1\text{kpc})^2$, where $M_\star(< 1\text{kpc})$ is computed from the best-fit Sersic profile to the surface density distribution.
- **$f_{\text{gas}}$, $\tau_{\text{depl}}$**: Gas-to-baryonic mass fraction $M_{\text{gas}}/M_{\text{bar}}$, and gas depletion time via star formation $M_{\text{gas}}$/SFR.
3. GLOBAL PROPERTIES OF STAR-FORMING GALAXIES AT $z \sim 2$

Along with the cosmically integrated evolution of the SFR, stellar mass, and SMBH accretion rate density (Madau & Dickinson 2014), a key outcome of lookback surveys was to reveal and establish the existence of scaling relations between global properties of galaxies out to at least $z \sim 2.5$, and a census of how they are populated (often quantified by galaxy type). In what follows, we first address the build-up of stellar mass in galaxies. Section 3.1 considers the scaling relation between the (in-situ) growth rate (SFR) and its time integral ($M_\star$, including effects of stellar mass loss and merging), followed by an overview of results on census (Section 3.2) and a discussion on the interpretation of these joint observational constraints (Section 3.3). We then expand our scope to include global structural measures (Section 3.4), ISM probes (Sections 3.5 - 3.6) and nuclear activity (Section 3.7).

### 3.1. The “Main Sequence” of Star-forming Galaxies

Locally, the existence of a strong correlation between the SFR and stellar mass of galaxies was first established based on the vast number statistics offered by the Sloan Digital Sky Survey (SDSS; Brinchmann et al. 2004). Subsequent work on deep lookback surveys revealed that a similarly tight and near-linear relation, dubbed the “Main Sequence,” was already in place since $z \sim 2$ (Noeske et al. 2007, Elbaz et al. 2007, Daddi et al. 2007). Its main change with cosmic epoch is one of rapid zero-point evolution. For galaxies below $10^{10} \, M_\odot$ the specific SFR evolves as $sSFR \propto (1+z)^{1.9}$ whereas more massive galaxies exhibit a faster pace of evolution, with $sSFR \propto (1+z)^{2.2-3.5}$ for $\log(M_\star/M_\odot) = 10.2 - 11.2$ (Whitaker et al. 2014).

The past few years have seen a consolidation of the MS relationship, leading to an emerging picture in which (a) the scatter is constant at $0.2 - 0.3$ dex over the full stellar mass and redshift range probed, (b) the low-mass slope is consistent with unity, and (c) a turnover and flattening is evident at higher masses, most prominently so towards lower redshifts and conversely nearly vanishing by $z \sim 2$ (e.g., Whitaker et al. 2013, Schreiber et al. 2015, Tomczak et al. 2016, Figure 4). Some studies favor or adopt single powerlaw fits (Speagle et al. 2014, Pearson et al. 2018), then finding its slope to steepen with increasing redshift.

Quantitative differences in derived scatter, slope/shape and normalization can be attributed to a range of reasons, including (1) method and strictness of SFG selection, (2) dynamic range over which the relation is fit, and (3) use of different SFR tracers. We briefly elaborate on these systematics before highlighting the significance of the MS scaling relation.

Whitaker et al. (2012) demonstrate how a $UVJ$ color selection vs. selecting only blue star-forming galaxies makes the difference between finding a sub-linear vs. linear slope. Similarly, Rodighiero et al. (2014) and Johnston et al. (2015) illustrate how, by adopting different color cuts or selection criteria based on SED-modeled properties, inferred slopes may vary between $\sim 0.8$ and $\sim 1$. Noteworthy also is that, when restricting samples to pure disks or considering only the disk components of SFGs, a slope of unity is found (Abramson et al. 2014). As we will allude to in Section 3.3, galaxies may well lack a bimodality in their sSFR distribution akin to that seen in their colors, implying that the choice of SFG selection criterion may largely be arbitrary. In this case there is no formally correct answer regarding the MS shape, and inferences on galaxy evolution need to treat the SFG and quiescent population jointly or at least preserve internal consistency in selection criteria used.

Unavoidably, the dynamic range in stellar mass over which the MS shape can be constrained is a function of redshift, with for example the ZFOURGE magnitude limit of $K_s = 25$ mag corresponding to $90\%$ completeness limits of $\log(M_\star/M_\odot) \sim 8.5, 9.5$ and 10.
Evolution of selected galaxy scaling relations and censuses from $z = 3$ to $z = 0.1$ (color-coded from red to purple as labeled in the panels). **Top row:** The first three panels show the MS of SFGs, the stellar mass function for all galaxies and for SFGs and quiescent galaxies (QGs) separately (thick and thin lines), consistently extracted from the same data set (Tomczak et al. 2014, 2016). The rightmost panel plots the molecular gas mass fraction from the scaling relations of Tacconi et al. (2020).

**Bottom row:** The two leftmost panels contrast the relationships between stellar mass, size, and stellar mass surface density within $r < 1$ kpc for SFGs and QGs, respectively (thick and thin lines; van der Wel et al. 2014a, Barro et al. 2017a). The next panel plots the stellar mass vs. gas-phase metallicity relation estimated via [NII]/Hα from Wuyts et al. (2014) and Zahid et al. (2014) (using the Pettini & Pagel 2004 calibration). The rightmost panel illustrates the evolution of the fraction of rotation-dominated SFGs (with ratio of intrinsic rotation velocity to velocity dispersion $> 1$) based on ionized gas kinematics (Kassin et al. 2012, Simons et al. 2017, Turner et al. 2017, Wisnioski et al. 2019). In the various panels, dashed lines indicate extrapolations in $M_\star$ and/or $z$ when no consistent measurements or fits were available.

Even with extreme depth and a consistent SFG definition, determinations of the MS scatter, normalization, and shape will be affected by uncertainties in the inferred SFRs and stellar masses. When the two are derived from overlapping data and sometimes a single modeling procedure, the uncertainties will be correlated and can potentially conspire to an artificially tight relation, compensating the opposite and mostly subtle boosting of scatter due to finite redshift bins that is not always accounted for. A comprehensive discussion of...
systematic uncertainties affecting estimates of SFR and $M_\star$ is presented by Conroy (2013, see also Supplemental Text, which summarizes the ingredients, assumptions, and challenges of spectral modeling techniques). Possible concerns include the saturation of reddening as a dust attenuation tracer at the highly star-forming and massive end (e.g., Wuyts et al. 2011a), extra extinction towards HII regions which remains difficult to pin down observationally (e.g., Reddy et al. 2015), contamination by other sources of emission such as AGN, circumstellar dust around asymptotic giant branch (AGB) stars or diffuse cirrus dust heated by old stellar populations, and unintended biases induced by the choice of adopted parameterization of and/or prior on the SFH (Carnall et al. 2019, Leja et al. 2019a).

Despite the above considerations, the meta-analysis by Speagle et al. (2014) finds a remarkable consensus among MS observations, with an interpublication scatter as small as 0.1 dex. On an individual galaxy basis different SFR estimates do of course vary more than that, but may not need to agree in detail either, as they can probe different timescales. H recombination lines are the closest to a measurement of the instantaneous SFR because of the short lifetime ($\sim 10$ Myr) of Lyman-continuum producing OB stars, while rest-UV and IR tracers will integrate the contribution of stars with (stellar) main sequence lifetimes of $\sim 100$ Myr. As such, differences in MS scatter inferred from different SFR tracers could in principle encode the short-term stochasticity of star formation and the timescale on which galaxies lose “memory” of previous activity (Caplar & Tacchella 2019). A slightly enhanced scatter around the H$\alpha$-based MS at cosmic noon relative to the one constructed from UV or UV+IR based diagnostics has been reported (Shivaei et al. 2015, Belli et al. 2017b), but systematic uncertainties regarding dust corrections make the interpretation in terms of star formation timescales not unique.

Setting aside the above caveats, we conclude this Section by noting two immediate implications of the existence of a MS relation and its observed evolution with cosmic time. First, assuming SFGs are located on the MS at all times we can integrate along the evolving scaling relation to recover the typical star formation history (SFH). Doing so, one unambiguously finds the star formation activity first rises before it falls, as such mimicking the shape of the cosmic SFR density evolution (Renzi 2009, Peng et al. 2010, Leitner 2012, Speagle et al. 2014, Tomczak et al. 2016, Ciesla et al. 2017). In common with findings from the fossil record (e.g., Thomas et al. 2005), these studies also infer SFHs of more massive galaxies to peak earlier. A second point of significance is that the tightness of the MS implies that any large excursions in star formation activity as one might expect from (major) merging have either very short duty cycles or are very rare (Rodighiero et al. 2011).

### 3.2. The Stellar Mass Function

An extensive body of work has documented the census of galaxies as a function of their stellar mass over most of cosmic history on the basis of well-sampled SEDs for deep, near-IR selected samples (e.g., Ilbert et al. 2013, Tomczak et al. 2014, see Figure 4). In common between these studies are the following findings. First, provided sufficiently deep stellar mass completeness limits a double-Schechter functional form is favored over a single-Schechter fit. This conclusion holds for both the star-forming and quiescent population individually, and for the combined, total galaxy stellar mass function. Second, between $z \sim 2$ and the present day there is no statistically significant evolution in the characteristic mass $M^*$ of either the total stellar mass function or that of SFGs (Peng et al. 2010). Values quoted in the literature for this characteristic mass vary in the range $\log(M^*/M_\odot) = 10.6 - 11$ with the higher results stemming from single-Schechter and the lower ones from double-Schechter.
fits (see, e.g., Tomczak et al. 2014). Minor differences further arise from the adopted fitting method (1/V\text{max vs.} maximum-likelihood), systematics in the determination of redshifts and stellar mass, and how uncertainties in the latter are accounted for. A third conclusion is that little to no evolution in the low-mass slope $\alpha \sim -1.5$ is noted since cosmic noon, neither for the total nor the star-forming galaxy population. Most of the evolution over the past 10 Gyr can thus be described by an increase in $\Phi^*$. The redshift-invariance of the low-mass slope $\alpha$ is in line with a MS slope of unity at masses below $\log(M_*/M_\odot) < 10.5$. As pointed out by Peng et al. (2010), a sub-linear MS slope would inevitably lead to a fast steepening of $\alpha$, and only very slight deviations from a unity slope can be accommodated by merging away low-mass galaxies. Whereas until recently inconsistencies at the level of 0.2 – 0.3 dex were found between integrating the MS metric and the evolving stellar mass function (Leja et al. 2015, Tomczak et al. 2016), which could not all be accounted for by merging, the latest such exercise with revised SFRs and stellar masses from advanced spectral modeling shows an improved internal consistency (Leja et al. 2019b).

As illustrated in Figure 4, the quiescent galaxy mass function looks markedly different. At all epochs it features a clear peak around $M^*$, and the quiescent population grows in numbers more rapidly than the star-forming one. At masses above $10^{10} M_\odot$ quiescent number densities have grown by a factor 6 since $z \sim 2$, whereas at lower masses there is a $15-30 \times$ increase. The mass-dependent growth of the quiescent population, with quenching of low-mass galaxies happening at later times (Ilbert et al. 2013, Huang et al. 2013), has been attributed to two different quenching channels. Since the environmentally driven low-mass channel only manifests itself appreciably after the epoch of cosmic noon, this review focuses on the high-mass quenching dominant at early times.

### 3.3. Interpreting the Observed Stellar Mass Growth

Whereas observational campaigns of the stellar mass growth across most of cosmic history have tightened the error bars on its scaling relation (the MS) and census (the galaxy stellar mass function), perhaps of more debate today is the interpretation of these observational diagnostics. That is, what are the implications of the cross-sectional view of the galaxy population at a range of epochs for the evolutionary tracks that individual galaxies follow?

In this context two schools of thought have developed which, to use the nomenclature of Abramson et al. (2015), can be described as “mean-based” and “dispersion-based” approaches. The former aim to reconstruct the average SFH of individual galaxies based on ensemble averages (e.g., Peng et al. 2010, Behroozi et al. 2013b), whereas the latter put emphasis on the diversity of SFHs (e.g., Gladders et al. 2013, Kelson 2014, Abramson et al. 2015, 2016). Both schools infer characteristic SFHs that first rise and then fall, but differ in key aspects of the interpretation.

Peng et al. (2010) for example adopt the redshift-invariance of $M^*$ as an indication that galaxies live on and grow along the evolving MS until they reach this critical mass, after which the probability of quenching increases rapidly $\propto 1 - e^{-M/M^*}$. Proposed mechanisms to explain this “mass quenching” include the rapid expulsion of gas by SMBHs, but there

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2 In the case of a double-Schechter fit, we here refer to the steeper of the two fitted slopes ($\alpha_1, \alpha_2$), which dominates at the low-mass end.

3 All modeling combining measures of SFR and stellar mass accounts for stellar mass loss, which reduces the mass present in stars (including remnants) compared to the integral over the SFH, by a factor 0.6 at late times for a Chabrier IMF.
is no consensus yet regarding its physical cause. Scatter around the MS is in such models typically attributed to short timescale ($\sim 10^{7-8}$ yr) variations in SFR at a given mass, induced by the breathing cycles of star formation feedback and temporal fluctuations in the rate of gaseous inflows and/or minor mergers.

The “dispersion-based” school on the other hand attributes scatter around the MS relation as an imprint of SFHs that are differentiated on Hubble timescales. In this picture galaxies follow smooth trajectories that let them pass across the moving MS, rather than at any time being stochastically scattered around the scaling relation. There is in such a scenario no discernable signature of quenching. That is, no rapid quenching mode and no specific time (other than arguably the peak in SFH) at which a shutdown in star formation is triggered. Along the same vein, Eales et al. (2014) report a continuous distribution of galaxies in the sSFR – $M_*$ space, lacking a bimodality in specific SFRs as undeniably seen in their color distribution. The color bimodality, they argue, reveals the peculiarities of stellar evolution (i.e., ageing stellar populations saturating in color) rather than a signature of galaxy evolution producing two sharply distinct populations of galaxies. A common interpretation in these studies is that the SFH shape is set by initial density conditions intimately related to dark matter (DM) properties such as the halo formation redshift. A family of log-normal SFHs, parameterized by varying peak times and widths, can yield an adequate description of the relevant observational metrics [Gladders et al. 2013, Abramson et al. 2015, 2016, Diemer et al. 2017], although the fact that the central limit theorem produces a similar relation between SFR and stellar mass within a framework in which galaxies grow stochastically illustrates that this inference is not unique [Kelson 2014, Kelson et al. 2016].

Speagle et al. (2014) present a hybrid approach in which average SFHs are derived by integrating the MS similar to what was done by Renzini (2009) and Peng et al. (2010), but its scatter is reproduced by imposing an initial spread in formation times to the smooth evolutionary tracks as opposed to adding short-term fluctuations in SFR at a given mass. Turning to numerical simulations of galaxy formation where the individual evolutionary paths of galaxies are by construction known, Matthee & Schaye (2019) argue that the MS scatter contains contributions from (slightly dominant) short-timescale self-regulation of star formation as well as halo-related variations on Hubble timescales. Of course, the precise contribution from short-timescale fluctuations may depend on the detailed recipes implemented in the numerical simulation.

A promising path forward to discriminate between the two schools of thought is to look for correlations between the offset from the MS midline and other SFG properties that can be assumed to vary more slowly over time, such as galaxy structure. Absence of a correlation within the MS scatter would then favor a short-timescale origin whereas a correlation between MS offset and longer lasting features would favor a Hubble-timescale differentiation. This requires accurate SFR measurements, where possible contrasting MS offsets quantified using multiple SFR tracers (e.g., Fang et al. 2018), ideally with different timescale sensitivities (Caplar & Tacchella 2019). Given challenges posed in this regard by dust treatment, we conclude that SFRs and stellar masses by themselves may ultimately prove insufficient to recover the underlying evolutionary paths of galaxies. Progress thus entails incorporating the information provided by spatially resolved studies of the build-up of galaxies in all their baryonic components (stars, gas, metals), tied with kinematic tracers of the full gravitational potential (i.e., including DM) and of the feedback processes at play. In the remainder of this Section, we cover the global structure, ISM, and accretion scaling relations, to delve more into resolved properties in Section [4].

DM: Dark matter.
3.4. The Mass-Size Relation

Following initial work with HST on the sizes of the UV-selected subpopulation of SFGs (Giavalisco et al. 1996, Ferguson et al. 2004), size evolution of mass-complete samples since cosmic noon was first explored in large numbers using ground-based near-IR surveys (Franx et al. 2008, Williams et al. 2009), to be transformed by rest-optical imaging at high resolution for statistical samples after the installment of WFC3 onboard HST. This Section focuses on stellar light-weighted sizes. Insights gained from a multi-tracer analysis combining stellar mass-weighted sizes and radial distributions of star formation, gas, and dust are covered in Section 4.1.

Even when concentrating on a single tracer/wavelength, multiple definitions of galaxy size are possible, and increasingly explored alongside one another. Different methods classify broadly as parametric and non-parametric. By far the most common approach entails fitting of a parametric (usually Sérsic) functional form convolved with the point spread function to the two-dimensional (2D) surface brightness distribution, and adopting the radius enclosing 50% of the light (a.k.a. the effective radius) as size measure, either defined along the major axis or in circularized form \( R_{e,\text{circ}} = \sqrt{b/a} R_e \). Variations include quantifying galaxy size based on a different percentile (e.g., \( R_{80} \)) or decomposing the light distribution in multiple components (e.g., bulge and disk) with a size associated to each. Non-parametric approaches range from curve of growth analyses to quantifying the pixel area above a given surface brightness threshold. The former requires a center and aperture definition, whereas the latter is designed to function well also for highly irregular morphologies but requires accounting for cosmological surface brightness dimming and luminosity evolution. Unlike the parametric approach that applies forward modeling of point spread function (PSF) smearing, the finite resolution is to be accounted for a posteriori in these non-parametric measures, typically using a simulation-based lookup table as correction factors are size and profile shape dependent. Here, we outline the main inferences from conventional Sérsic fitting, but note in passing how some conclusions change, even on a qualitative level, when adopting an alternative definition of size.

The sizes of star-forming and quiescent galaxies both show a tight (< 0.2 dex intrinsic scatter) but distinct scaling with galaxy stellar mass (van der Wel et al. 2014a, see Figure 1). SFGs are larger than their quiescent counterparts at all masses over the 0 < z < 3 range. Their size-mass relation exhibits a non-evolving slope of \( \frac{d \log R_e}{d \log M_*} = 0.22 \) compared to the steeper slope of \( \frac{d \log R_e}{d \log M_*} = 0.75 \) for early-type galaxies. Considering the redshift dependence of the intercept, a slower evolution in the average size of the population at fixed mass is quantified for SFGs \( R_e \propto (1 + z)^{-0.75} \) compared the quiescent systems, which as a population show dramatic growth from compact red nuggets at cosmic noon to the large ellipticals in today’s Universe \( R_e \propto (1 + z)^{-1.48} \). Of note is that the above characterizes the evolution in the size distribution of the population, not by itself the evolutionary tracks of individual galaxies. Connecting progenitor-descendant sequences based on their constant cumulative number density as outlined in Section 2.5, information from the evolving galaxy stellar mass function can be folded in together with the size measurements to infer that: (1) the progenitors of present-day Milky Way mass galaxies have evolved, on average, along individual growth tracks of \( \frac{\Delta \log R_e}{\Delta \log M_*} = 0.27 - 0.3 \) (i.e., an inside-out growth track slightly steeper than the slope of the star-forming size-mass relation at any epoch; van Dokkum et al. 2013, 2015); and (2) the most massive galaxies have experienced much steeper size growth with individual tracks following \( \frac{\Delta \log R_e}{\Delta \log M_*} = 2 \), consistent with scenarios where an
**DARK MATTER HALO AND RELATED PROPERTIES**

- **$r_{200}$**: Virial radius of a DM halo, usually the radius within which the mean mass density is 200 times the critical density for closure of the Universe at the redshift of interest; also denoted $R_{\text{vir}}$ (Mo et al. 1998).
- **$\lambda$**: Spin parameter of a DM halo (Bullock et al. 2001).
- **$M_{\text{DM}}$, $J_{\text{DM}}$, $j_{\text{DM}}$**: Mass of a DM halo, and its total and specific angular momentum at the virial radius (with $j_{\text{DM}} = J_{\text{DM}}/M_{\text{DM}}$).
- **$m_d$, $j_d$**: Mass and angular momentum of the baryonic disk galaxy expressed as fractions of the host DM halo mass and angular momentum (such that $M_{\text{bar}} = m_d M_{\text{DM}}$, $J_{\text{bar}} = j_d J_{\text{DM}}$).

The early dissipative core formation phase is followed by the build-up of profile wings through dissipationless, predominantly minor, mergers (van Dokkum et al. 2010, Patel et al. 2013a).

The formation of galactic disks is inherently linked to the DM halos that host them. In its simplest form, disk scalelengths are expected to scale with the virial radii of their host halos as:

$$R_d = \frac{1}{\sqrt{2}} \left( \frac{j_d}{m_d} \right) \lambda r_{200},$$

which boils down to a linear scaling with the virial radius $r_{200}$ provided the accreting baryons retain the specific angular momentum of their host halo ($j_d/m_d = 1$; Mo et al. 1998). The width of the log-normal distribution in spin parameters $\lambda$ obtained from N-body simulations in a ΛCDM cosmology (Bullock et al. 2001) is sufficient to account for the observed scatter in the size-mass relation. Such a scenario predicts an evolution in size at fixed halo mass following $R \propto H(z)^{-2/3}$, in agreement with the observed evolution for late-type galaxies by van der Wel et al. (2014a), who note that a parameterization as a function of $H(z)$ is marginally favored over that with the scale factor $(1 + z)$. Adopting the stellar mass - halo mass (SMHM) relation inferred from abundance matching, the observed size - mass relation can be converted to a galaxy size - halo size relation (Kravtsov 2013, Huang et al. 2017, Somerville et al. 2018). Applied to observations at $0 < z < 3$, such analyses reveal a linear relation between $R_e$ and $r_{200}$, and hence evidence for homologous growth between galaxies and their host halos. At least at $0.5 < z < 3$ the normalization for late-type galaxies is consistent with expectations from simple disk formation models (see also Section 4.4.4 for kinematic evidence of specific angular momentum retention in an ensemble-averaged sense). The effective radii of early-type galaxies on the other hand lie below the relation at all epochs. Mowla et al. (2019a) however suggest that expressed in $R_{80}$ quiescent galaxies and SFGs occupy a single size-mass relation, with these outer size measurements exhibiting a close relationship to the host halos for the full population. Whereas observations and simulations agree on a general linear relation of the form $R_d = A r_{200}$, recent theoretical work has called into question whether the proportionality constant $A$, and hence the variation in galaxy size at fixed mass, is set by the halo spin parameter $\lambda$ as in equation 1, halo concentration (Jiang et al. 2019), or a combination of both (Somerville et al. 2018).  

Key in the above results is that they are based on mass-complete samples of galaxies. Individual sub-populations may differ in their growth rate. Allen et al. (2017) report a significantly faster size growth for Lyman break galaxies (LBGs; $R_e \propto (1 + z)^{-1.2}$) than for the underlying full SFG population since $z \sim 7$, a trend also seen in previous studies spanning a more modest redshift range, implying that LBGs represent a special subsample...
of highly star-forming and compact galaxies. Population differences aside, Ribeiro et al. (2016) report for the same sample of spectroscopically confirmed SFGs at $2 < z < 4.5$ differences in size evolution at fixed mass ranging from $R_e \propto (1 + z)^{-1.4}$ using conventional Sérsic profile fits to no size evolution at all over the considered 2 billion years leading up to cosmic noon when adopting a non-parametric measure of size quantified based on the pixel count above a threshold surface brightness. They attribute this to galaxies in their earliest phase of assembly being quite extended and irregular, and poorly described by a single Sérsic profile. An example at later epochs where alternative size definitions change trends in a qualitative manner includes work by Carollo et al. (2013) who adopt curve-of-growth sizes with a posteriori PSF correction factors to conclude, at odds with van der Wel et al. (2014a), that there is no decline in number densities of compact quiescent galaxies since $z < 1.5$, thus placing more emphasis on progenitor bias than individual galaxy growth as an explanation of the observed size evolution of early-type galaxies.

### 3.5. Cold Gas Content

The cold gas reservoir of galaxies lies at the core of their evolution, fueling their star formation activity and SMBH growth, and efficiently mediating mass, angular momentum, and energy transfer. CO line or far-IR to $\sim 1 \text{ mm}$ dust continuum observations have accumulated ample evidence that SFGs at cosmic noon have copious amounts of molecular gas (see reviews by Combes 2018, Tacconi et al. 2020). A recent focus has been on scaling relationships described in relation to the MS, facilitating the interpretation in the framework of galaxy evolution and providing well-calibrated recipes to estimate $M_{\text{gas}}$ in the absence of actual cold ISM measurements (e.g., Genzel et al. 2015, Scoville et al. 2017, Tacconi et al. 2018). These analyses showed that over $z \sim 0 − 4$ the depletion time $\tau_{\text{depl}} = M_{\text{gas}}/\text{SFR}$ depends primarily on redshift and MS offset $\Delta MS = \log(\text{sSFR}/\text{sSFR}_{\text{MS}}(M_\star, z))$, and so does the ratio of molecular gas to stellar mass $\mu_{\text{gas}}$ with an additional dependence on $M_\star$. In the updated derivation by Tacconi et al. (2020), unifying CO and dust continuum-based gas mass estimates including most recent NOEMA and ALMA data, and adopting the Speagle et al. (2014) MS parametrization, $\log(\tau_{\text{depl}}) = 0.21 - 0.98 \log(1 + z) - 0.49 \Delta MS + 0.03 \log(M_\star/M_\odot) - 10.7$. Accordingly, the depletion time for MS SFGs at fixed $M_\star$ increases by a factor of $\sim 3$ from $z = 2$ to the present day while the gas fraction $f_{\text{gas}} = M_{\text{gas}}/(M_\star + M_{\text{gas}})$ drops by a factor of $\sim 10$ (Figure 4). It also follows from these gas scalings, the near-linear MS and its evolution (from Speagle et al. 2014), and the size-mass relation for SFGs (from van der Wel et al. 2014a), that the gas mass surface density at fixed $M_\star$ evolves strongly over $0 < z < 2$ as $\Sigma_{\text{gas}} \propto (1 + z)^a$ with $a \sim 4$, and more slowly at $2 < z < 4$ with $a \sim 2$.

At all epochs, the average gas depletion time is nearly ten times shorter than the Hubble time, requiring sustained replenishment of the galactic cold gas reservoirs to maintain the SFG population as a whole on the tight observed MS. As summarized by Tacconi et al. (2020), this argument is a cornerstone of the “equilibrium growth” model, and favors that the bulk of SFGs are fed by smoother gas accretion modes via cold streams along the cosmic web and minor mergers rather than major mergers. At fixed $M_\star$ and $z$, the gas scaling relations imply that the enhanced SFRs well above the MS are driven by both higher gas fractions and higher star formation efficiencies ($1/\tau_{\text{depl}}$), plausibly reflecting increased gas accretion and concentration as, e.g., in a major merger event. On the MS, the star formation efficiency is roughly constant but $f_{\text{gas}}$ decreases towards higher masses, along with the sSFR, suggesting that a lack of fuel (resulting from, e.g., suppressed accretion or
gas removal) sets quenching on rather than reduced efficiency (from, e.g., gas stabilization against fragmentation by a massive bulge or ISM heating mechanisms). Setting tighter constraints on these scenarios through measurements of the cold ISM in sub-MS galaxies at z > 1 is very challenging, and the very few results published to date are inconclusive (e.g., Bezanson et al. 2019).

Gas scaling relations at z > 1 are most firmly established at log(M_*/M_⊙) > 10, where high-z samples probe well the SFG population and where the luminosity-to-gas mass calibrations are best constrained. The more extensive data sets now available do not support a significant dependence of the CO-H_2 conversion on ∆MS (Tacconi et al. 2020). In contrast, there is a strong variation of CO-H_2 and of the dust-to-gas ratio with metallicity (e.g., Genzel et al. 2012, Bolatto et al. 2013), which is folded in the scaling relations given above. At z > 0.5, the atomic gas contribution to M_gas on galactic scales is generally neglected (though a 36% correction for He is applied) since most of the hydrogen is expected to be in molecular form at the high densities inferred (> 10 M_⊙ pc^{-2}) and Damped Lyman α Absorbers studies indicate a slow evolution in H_I gas density (∝ (1 + z)^{0.57}; Péroux & Howk 2020).

3.6. Metallicity and ISM Conditions

The metal content of galaxies is a sensitive probe of the baryon cycle, carrying the imprint of gas accretion, stellar nucleosynthesis, galactic winds, and internal gas mixing. Observational constraints for z ~ 2 SFGs have largely come from strong rest-optical nebular emission lines, interpreted through empirical and/or theoretical calibrations in terms of the gas-phase oxygen abundance (O/H). These lines also depend on the nebular conditions and structure, and on the excitation sources, affecting calibrations. The reviews by Maiolino & Mannucci (2019) and Kewley et al. (2019) discuss in detail the strengths and limitations of various indicators, and stress the importance of combining multiple diagnostics, of adopting the same method(s) to reduce the impact of systematic differences in calibrations, and of using consistent approaches in deriving galaxy properties (M_*, SFR, ...) used to establish scaling relations.

Offsets in the location of (non-AGN) z ~ 2 SFGs relative to the z ~ 0 excitation sequences in line ratio diagrams have long been known (e.g., in [NII]λ6584/Hα and [SII]λλ6716, 6731/Hβ vs. [OIII]λ5007/Hβ, and ([OIII]λλ3726, 3729+[OII]λλ4959, 5007)/Hβ vs. [OIII]λ5007/[OII]λλ3726, 3729). The growing near-IR spectroscopic data sets at z ~ 2 have enabled a more systematic exploration of the origin of the observed offsets, providing evidence for evolving conditions of the ionized gas in terms of a harder ionizing radiation, elevated N/O abundance ratio, higher electron density and ISM pressure, and higher ionization parameter, at fixed O/H abundance (e.g., Masters et al. 2016, Steidel et al. 2016, Strom et al. 2018, Kashino et al. 2019). Other factors may be at play such as the presence of weak AGN activity, galactic-scale outflows and shocks, and diffuse ionized gas — the importance of which varies with redshift — as well as sample selection, and aperture and weighting effects where spectra of high- and low-z galaxies may encompass different physical regions and span a range of excitation (e.g., Shapley et al. 2015, 2019, Kaasinen et al. 2017, Sanders et al. 2017). Constraints on the electron density of ionized gas have also been obtained from the [OIII] and [SII] doublet ratio, pointing to an increase with redshift, with n_e in the range 100 – 400 cm^{-3} for z ~ 2 SFGs compared to ~ 25 cm^{-3} for z ~ 0 galaxies (e.g., Sanders et al. 2016a, Kaasinen et al. 2017). These estimates may be somewhat inflated by emission from denser gas in the ubiquitous galactic winds at z ~ 2 (Section 4.6) in the single-component line fits commonly performed.

n_e: Local electron density, the number of electrons per unit volume of an ionized nebula.

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Turning to metallicity, while the “strong line” methods based on nebular rest-optical emission can lead to systematic differences in log(O/H) by up to ~ 0.7 dex, relative estimates based on the same calibration are more accurate. The general shape and evolution of the mass-metallicity relation (MZR) agree qualitatively among various studies out to z ~ 3.5, with lower metallicities at lower $M_*$, an overall decline in metallicity at earlier times, and a stronger evolution in the low-mass regime, in agreement with the (scarcer) results from rest-UV metallicity-sensitive features in young stars (see Maiolino & Mannucci 2019). Among several proposed parametrizations, the form $12+\log(O/H) = Z_0 + \log \left[ 1 - \exp \left( -\left( M_*/M_0 \right)^\gamma \right) \right]$ is physically motivated based on considerations of the chemical yields in the presence of inflows and outflows. It describes well the bending shape of the MZR up to $z \sim 2.5$, where $Z_0$ is the asymptotic value at high mass and $M_0$ is the evolving turnover mass (with $M_0 \propto (1+z)^\beta$, where $\beta \sim 2.6 - 2.9$) below which the relation follows a power law of index $\gamma \sim 0.4 - 0.6$ (e.g., Zahid et al. 2014, Wuyts et al. 2014, and references therein; see Figure 1).

A secondary dependence on the SFR, ultimately tied to the gas fraction, is expected in a theoretical framework, where accretion of metal-poor gas dilutes the galactic gas-phase metallicity while increasing the gas reservoir fueling star formation. Based on the large set of SDSS local galaxy spectra and first results at high z, Mannucci et al. (2010) proposed a redshift-invariant fundamental metallicity relation (FMR) between log(O/H), $M_*$, and SFR, parametrized in terms of $\log(M_*) - \alpha \log(SFR)$. While subsequent work at high z has led to mixed results possibly due to the limited dynamic range and uncertainties in SFRs, a consensus is now emerging for the detection of a FMR albeit with hints of a modest evolution with lower log(O/H) at fixed $M_*$ and SFR to $z \sim 2.5$, and possibly stronger evolution at $z \gtrsim 3$ (e.g., Sanders et al. 2018, Maiolino & Mannucci 2019). Such an evolution may reflect a progressive increase of the mass loading factor $\eta$ of galactic winds (the ratio of mass outflow rate to SFR) and/or decrease of the metallicity of inflowing gas with lookback time; beyond $z \sim 3$, infall rates of more pristine gas may overwhelm metal production through stellar nucleosynthesis, resulting in stronger dilution. Theoretical models and numerical simulations that match the observed MZR, FMR, and evolution thereof underscore the role of stellar feedback in the chemical evolution of galaxies, requiring an increasing $\eta$ in lower-mass galaxies and winds removing gas at roughly the same rate as consumed by star formation around $\log(M_*/M_\odot) \sim 10$ (e.g., Erb 2008, Lilly et al. 2013, Muratov et al. 2015, Davé et al. 2017). More direct observational constraints on $\eta$ at $z \sim 2$ will be discussed in Section 1.6.2.

### 3.7. AGN Demographics

The link between the growth of galaxies and their SMBHs, deduced from local scaling relations and the co-evolution in cosmic SFR and black hole accretion rate densities, has motivated an abundant literature on AGN activity and feedback across cosmic time (e.g., Fabian 2012, Heckman & Best 2014, Lutz 2014, Brandt & Alexander 2015, Padovani et al. 2017 for reviews). We summarize key aspects on the demographics of radiative-mode AGN at high z.

AGN, identified at X-ray and other wavelengths, are preferentially found in higher mass galaxies, which, for an underlying positive correlation between AGN luminosity and host mass, reflects flux limits in the data from which AGN are identified. Comparisons of the host properties of X-ray-selected AGN with those of mass-matched samples of inactive galaxies showed that AGN reside mainly in MS SFGs with little correlation between X-ray luminosity $L_{X,\text{AGN}}$ and SFR, are rarely associated with disturbed morphologies, but are...
more prevalent in hosts with denser stellar cores (e.g., Silverman et al. 2009, Kocevski et al. 2012, 2017, Mullaney et al. 2012a, Santini et al. 2012). The lack of correlation between $L_{\text{X,AGN}}$ and SFR is understood in terms of the short-term $\lesssim 10^6$ yr variability of AGN compared to the $\gtrsim 10^8$ yr timescales of galactic star formation processes (e.g., Hickox et al. 2014). X-ray stacking analyses, effectively averaging over time, revealed a closer connection between inferred SMBH accretion rate and host SFR (e.g., Mullaney et al. 2012b). The ratio of average SMBH accretion rate to SFR appears to be largely independent of galaxy stellar mass, and so is the distribution of specific $L_{\text{X,AGN}}$ (often taken as a proxy for the Eddington ratio; e.g., Aird et al. 2012, 2018). While the distribution in specific $L_{\text{X,AGN}}$ shifts to higher values towards higher $z$, a mass-independent distribution at fixed $z$ implies that a wider range of $L_{\text{X,AGN}}/M_\star$ is probed at higher host mass. AGN selected by rest-optical and mid-IR diagnostics are less prone to variability effects but susceptible to similar biases related to “dilution” by host galaxy emission (e.g., Padovani et al. 2017). A longer term connection between $L_{\text{X,AGN}}$ and SFR, coupled with evidence from morphologies, is consistent with a picture in which $z \sim 2$ AGN are fueled by stochastic accretion, and secular processes (rather than major mergers) within the gas-rich hosts promote the growth of both SMBH and a central bulge (e.g., Mullaney et al. 2012b). The exception might be for the most luminous and most obscured mid-IR-selected AGN, underrepresented in X-ray surveys, whose morphologies are significantly more frequently disturbed or indicative of merging (Donley et al. 2018).

Observations, as well as theoretical models and cosmological simulations (e.g., Somerville & Davé 2015, Naab & Ostriker 2017) support a link between AGN and star formation quenching at high masses. Causality, however, remains so far elusive. Empirical connections through galactic structure and outflows are discussed in Sections 4.1 and 4.6.

4. RESOLVED PROPERTIES OF STAR-FORMING GALAXIES at $z \sim 2$

Our understanding of the processes driving the evolution of the global galaxy properties discussed above has greatly benefitted from the growing amount of data resolving individual galaxies. A key finding was that high $z$ SFGs are predominantly disks, albeit more turbulent than local spirals. The growth and evolution of disks as derived from stellar light, star formation, and kinematic tracers is first discussed (Sections 4.1 - 4.3), followed by emerging dynamical constraints on the interplay between baryons and DM on galactic scales (Section 4.4) and deviations from disk rotation (Section 4.5). Non-gravitational motions (i.e., gas outflows) are then addressed, as direct probe of feedback in action (Section 4.6).

4.1. Star-Forming Galaxies as Axisymmetric Systems

4.1.1. Morphological disk settling and the emerging Hubble sequence. Many key features regarding the structural build-up of SFGs can be captured in a framework where we consider them as flattened, axisymmetric structures. This approach also fundamentally underpins semi-analytical models where any structural evolution is only described radially. Intrinsic 3D shapes inferred from projected axial ratio distributions illustrate how at any given epoch there is a tendency of increased fractions of SFGs with prolate (i.e., elongated) shapes in the low-mass regime, whereas the fraction of oblate (i.e., disky) systems increases with mass and toward later times (van der Wel et al. 2014b, Zhang et al. 2019). This downsizing pattern for morphological disk settling finds its counterpart in kinematic surveys,
which show similar mass and redshift dependencies for orderly rotating disk fractions, with dispersion-dominated systems gaining in prevalence toward lower masses (see Section 4.3 and Figure 4). This Section discusses the radial characteristics of SFGs with an emphasis on relatively massive ($\gtrsim 10^{10} M_\odot$) systems for which the axisymmetric disk framework is most appropriate. In the next Section we discuss how or where the actual morphology deviates from axisymmetry.

Salient features of the size-mass relation of SFGs were discussed in Section 3.4. The same HST surveys also shed light on surface brightness profile shapes, often quantified parametrically with a Sérsic model. For the MS population, exponential disk profiles of $n \sim 1$ are the norm (Wuyts et al. 2011b), in line with the disk-like nature inferred from axial ratios and kinematics. Exceptions arise more frequently at the very tip of the MS, and among the rare population of starbursting outliers above the MS, which on average are characterized by more centrally concentrated profiles. We can conclude that the overall structure quantified from rest-optical/UV light and colors correlates with location in the $M_\star - SFR$ plane, with most star formation happening in disks while quiescent galaxies feature cuspier profiles. A Hubble sequence, where the dominant morphology and stellar populations are intimately tied, can thus be said to be in place already since at least $z \sim 2.5$.

While it is most straightforward to compare sizes and profile shapes across epochs at fixed mass, individual galaxies build up stellar mass over time through star formation and mergers. Applying the cumulative comoving number density technique outlined in Section 2.3 progenitor-descendant sequences have been reconstructed to reveal the growth in size and build-up of extended profile wings around central cores for galaxies at the most massive end and to recover the structural growth history of Milky Way progenitors (van Dokkum et al. 2010, 2013, see also Patel et al. 2013b). The latter feature a more modest size growth and at least at $1 < z < 2.5$ a more self-similar evolution in profile shape than the most massive galaxies which increase rapidly in Sérsic index.

Other than by disentangling the population growth from growth of individual systems, major advances in our understanding of structural evolution are arising from comparing multiple tracers. Initially, this focused on rest-UV to rest-optical stellar emission, but increasingly this is complemented by resolved probes of ionized and molecular gas as well as reprocessed emission by dust.

### 4.1.2. Stellar mass distributions

With resolved imaging sampling the distribution of stellar light below and above the Balmer/4000Å break out to $z \sim 2.5$ a picture has emerged in which negative color gradients (i.e., redder centers than outskirts) become increasingly prominent towards the high-mass end and at later times (e.g., Liu et al. 2017, 2018). The age-dust degeneracy in a space of mass-to-light (M/L) ratio vs. rest-optical color (e.g., Bell & de Jong 2001) allows for a relatively robust translation of the multi-band light maps to a stellar mass distribution (Wuyts et al. 2012, Szomoru et al. 2013, Tacchella et al. 2015, Wang et al. 2017, Suess et al. 2019, see Figure 5). In common to such studies is the finding of more compact and centrally concentrated stellar mass profiles compared to those observed in light, especially at lower redshifts and higher masses. Carrying out bulge-disk decompositions on stellar mass maps, Lang et al. (2014) find that while SFGs are well described by exponential disks at low masses, once crossing the Schechter mass they already contain 40-50% of their stars in a bulge component, even prior to their eventual quenching. Overall, taking both SFGs and quiescent galaxies together, it is now well established that measures of bulge prominence or central surface density (e.g., $\Sigma_{1kpc}$; Cheung et al. 2012, Barro et al. 2014)
2017a, see Figure 4) form much more reliable predictors of quiescence than stellar mass by itself. However, the origin of this strong correlation, in particular its interpretation in terms of a causal connection, remains debated (Lilly & Carollo 2016, Abramson & Morishita 2018). Building on the increased prevalence of AGN with host central stellar mass density and the empirical inference that quenching sets on when the cumulative radiative energy of SMBHs reaches $\sim 4 \times$ the halo binding energy, Chen et al. (2020) recently put forward a phenomenological model that strengthens the role of AGN in quenching by explaining naturally the structural differences between star-forming and quenched galaxies.

4.1.3. Observed Hα profiles. WFC3 grism surveys such as 3D-HST (Momcheva et al. 2016) give access to the Hα surface brightness distributions on kpc scales for galaxies out to $z \sim 1.5$. Such observations have illustrated that the Hα emission of MS galaxies, tracing the unobscured instantaneous star formation, follows on average exponential disk profiles (Nelson et al. 2013), and that there is a resolved equivalent of the MS, a correlation between the local star formation and stellar surface density (Wuyts et al. 2013; see also Wang et al. 2017). Deviations from this relation are seen in the centers of particularly massive – SFGs, with also asymmetric features such as clumps contributing to the scatter (Section 4.2). Stacking Hα and H140 maps of 3200 $z \sim 1$ SFGs Nelson et al. (2016b) find the (unobscured) star formation to be slightly more extended than the stellar continuum emission, with a weak dependence on mass: $R_{e,H\alpha}/R_{e,H} = 1.1 \left( M_*/10^{10} M_\odot \right)^{0.054}$. Translated to Hα equivalent widths (EWs) this results in centrally dipping profiles, with the central depression in Hα EW being most prominent at the high-mass end. AO-assisted IFU surveys were able to push resolved Hα EW measurements out to $z \sim 2.5$, resulting in qualitatively similar findings (Tacchella et al. 2015). With such numbers at present limited to a few dozen (fewer when considering the high-mass end alone) and accumulated at a rate of $\sim$ one 8-m telescope night per object, significant progress on number statistics here is anticipated from grism observing modes on JWST. Already with existing ground-based (yet seeing-limited) instrumentation, however, larger samples with consistent continuum and Hα size measurements over the full $0.6 < z < 2.6$ range can be compiled. Doing so, Wilman et al. (2020) find an average size ratio of $R_{e,H\alpha}/R_{e,F160W} = 1.26$, without significant dependence on the redshift, mass and star formation activity. Adopting the observed size ratio as an upper limit to $R_{e,F160W}$, (a limit due to the possible presence of differential extinction and dust gradients), they infer the associated size growth due to star formation alone to proceed along a vector of $\frac{d \log R_e}{d \log M_*} \sim 0.26$, consistent with results from constant comoving number density arguments and only slightly steeper than the observed slope of the size-mass relation at any epoch. Other processes than simply adding new stars, such as feedback, angular momentum redistribution, (minor) mergers and the preferential quenching of more compact SFGs may need to be invoked to reconcile the relatively slow growth due to star formation with the observed size evolution of SFGs.

4.1.4. Attenuation gradients. In the absence of dust all of the above radial profiles, size differences, and red centeredness would be attributed most straightforwardly in terms of stellar population age (or sSFR) gradients consistent with a picture of inside-out disk growth. SFGs at cosmic noon however are far from dust free, particularly in the massive and highly star-forming regime where most of the internal color dispersion (e.g., Boada et al. 2015) and radial gradients are seen. With only a single rest-optical color, the effects of age and dust are fully degenerate. While this enables a robust estimate of spatial M/L ratio variations, explaining the origin of these variations (spatially inhomogeneous SFH vs. extinction) is by

EW: Equivalent width, for an emission line equal to the ratio of line flux to continuum flux density.
the same token a challenging task. Several approaches have been pursued to pin down to which degree levels of extinction vary across galaxy disks. Wuyts et al. (2012) used resolved SED modeling of 7-band ACS+WFC3 photometry to constrain the stellar populations of individual pixel bins in 0.5 < z < 2.5 SFGs. Nelson et al. (2016a) were able to extract a more direct probe of extinction for z ∼ 1 SFGs in the form of the Balmer decrement (Hα/Hβ), although relying on stacked profiles for relatively broad bins in stellar mass. Complementary broadband approaches further include use of the dust-sensitive UV slope β (Tacchella et al. 2018) and a rest-frame UVI color-color diagram (Wang et al. 2017, Liu et al. 2017).

While quantitative differences remain and direct comparisons are complicated by differences in applicable redshift range and technique (e.g., individual galaxies vs. stacking), a converging picture is emerging. Galaxies do feature radial gradients in extinction, with the amount of central enhancement increasing with stellar mass, reaching ∼ 2 magnitudes of central extinction at the high-mass end. Propagating this knowledge to the reconstruction of sSFR profiles yields on average surprisingly flat profiles over the full radial range for intermediate mass galaxies. Only among the most massive galaxies central drops in the star formation activity remain present after dust correction, a trend that is interpreted as a signature of inside-out quenching. For example, Tacchella et al. (2018) exploit near-IR AO-assisted IFU data at z ∼ 2 to find a radially constant mass-doubling timescale of ∼ 300 Myr for SFGs below 10^{11} M⊙, and central star formation suppression by a factor of ∼ 10 above this mass. At z ∼ 1, Wang et al. (2017) report qualitatively similar results with flat sSFR profiles for SFGs below 10^{10.5} M⊙ and central declines of 20-25% above this mass.

4.1.5. Compact dusty cores and implications for SFR profiles. Having highlighted the significant role of dust, it is important to underline the potential offered by far-IR to radio observations to complement our view of where star formation is happening (as seen reprocessed by dust) and where within the disks cold gas, the fuel for star formation, resides (as revealed by CO line emission). Here, ALMA, NOEMA and the JVLA with their recently enhanced sensitivities and long baselines are making major contributions. In low-J CO transitions, MS galaxies feature a similar extent as observed in the (rest-)optical. This appears to be the case both at z ∼ 1 (Tacconi et al. 2013) and z ∼ 2 (Bolatto et al. 2012).
although numbers in the higher redshift bin remain limited. A different picture is painted when considering continuum probes of star formation. Comprised predominantly of non-thermal synchrotron radiation from charged particles accelerated within supernova remnants, 1.4 GHz continuum emission serves as a dust-unbiased SFR tracer (Condon 1992). Using a uv-stacking algorithm to trace the 1.4 GHz continuum size evolution of \( \sim 1000 \) MS SFGs with \( 10^{10} - 10^{11} \) M\(_{\odot}\) spanning \( 0 < z < 3 \), Lindroos et al. (2018) find the measured radio sizes to be typically a factor of two smaller than those measured in the rest-optical. Likewise, focusing on thermal dust emission from a sample of normal MS galaxies at \( \log(M_*/M_\odot) \gtrsim 11 \), Tadaki et al. (2017a) combined ALMA 870 \( \mu \)m observations in compact and extended configuration to infer that the dust sizes of their targets were more than a factor of two smaller than those observed at rest-optical (and even more so H\( \alpha \)) wavelengths.

These results are in contrast to what naively would be anticipated given the typical centrally declining H\( \alpha \) EWs in the same high-mass regime at \( z \sim 2 \), even after dust corrections. Star formation happening in such centrally concentrated cores could in several hundred Myr build up a central bulge with \( \Sigma_{1\text{kpc}} > 10^{10} \) M\(_{\odot}\) kpc\(^{-2}\), akin to the central densities of lower redshift quiescent systems. Resolved maps at a second, higher frequency IR wavelength are needed to rule out or reveal any negative gradients in dust temperature that may bias the inferred half-SFR sizes to low values. In the handful of objects where resolved CO and dust continuum measurements are both available, authors also noted the smaller dust compared to CO sizes (Spilker et al. 2015, Tadaki et al. 2017b). Rujopakarn et al. (2016) on the other hand found 5 cm and 1.3 mm sizes of somewhat lower mass (\( \log(M_*/M_\odot) \sim 10.7 \)) SFGs at the same redshift to both be comparable to the extent of the stellar mass maps. Enhancing the robustness of multi-tracer structural measurements and interpreting the relative sizes of dust, stellar, and H\( \alpha \) emission as a function of mass stands as an important challenge for future studies. This applies especially to reconciling the apparently inconsistent findings from cold ISM and H\( \alpha \) observations at the massive end. At present, ambiguity remains whether this is due to uncertain dust corrections or instead differences between samples that fit into a common evolutionary sequence where massive galaxies undergo compaction events triggering nuclear starbursts (responsible for the compact dust sizes) followed by a phase of inside-out quenching (responsible for the centrally declining H\( \alpha \) EWs; e.g., Tacchella et al. 2016).

### 4.2. Deviations from Axisymmetry

#### 4.2.1. Shapes and morphologies.

Thus far, we discussed the structural properties of high-z SFGs in terms of sizes and radial profiles. Skewed axial ratio distributions for low-mass (\( \log(M_*/M_\odot) < 10 \)) SFGs at cosmic noon suggest that a framework of flattened axisymmetric disks may be inappropriate for young systems that have not had the time to settle into an equilibrium disk configuration (Law et al. 2012b, van der Wel et al. 2014b). Modeling the joint distribution of projected axis ratios and sizes, and accounting for the finding that smaller SFGs are systematically rounder, Zhang et al. (2019) argue that prolate and/or spheroidal shapes may in fact be even more common than inferred by van der Wel et al. (2014b), also for the \( \log(M_*/M_\odot) = 10 - 10.5 \) regime. They report young, low-mass galaxies in the VELA set of high-resolution hydrodynamical cosmological zoom-in simulations to be prolate as well. Kinematics reveal a qualitatively similar trend, with a threshold mass for disk settling that decreases with decreasing redshift (Section 4.3).

Even above \( 10^{10} \) M\(_{\odot}\), the morphological appearance of high-z SFGs often looks markedly different from that of the relatively smooth disk population in the local Universe.
Figure 5
Stellar structure and kinematics of 250 massive SFGs at cosmic noon. Left: Stellar mass maps derived from spatially-resolved SED modeling of multi-band HST imaging (Lang et al. 2014). Blue to red colors correspond to increasing stellar mass surface density, with the same range shown for all objects. Right: Velocity fields from Hα obtained with the VLT/KMOS multi-IFU instrument as part of the KMOS3D survey (Wisnioski et al. 2019), at a resolution of ~ 4 kpc. Blue to red colors correspond to the maximum blueshifted to redshifted velocities relative to systemic, adjusted individually for each object. The galaxies are plotted as a function of their $M_*$ and SFR (normalized to the SFR of the MS at log($M_*/M_\odot$) = 10.5 at the redshift of each object, shown as light grey thick line). The stellar mass maps are relatively smooth and show an increasing bulge prominence towards higher masses. The kinematics show an overall majority of rotating disks.

Rising fractions of irregular morphologies were first noted in early HST observations probing the rest-UV (Griffiths et al. 1994, Windhorst et al. 1995, Abraham et al. 1996), and later quantified using the larger samples provided by rest-optical legacy surveys such as CANDELS (e.g., Conselice 2014, Huertas-Company et al. 2016). Methods to quantify the evolving morphological mix through cosmic time encompass non-parametric morphological measures (e.g., concentration, asymmetry, Gini, M20; Conselice 2003, Lotz et al. 2004) or Principal Component Analysis thereof (Peth et al. 2016), visual classifications by experts or citizen scientists (e.g., Kartaltepe et al. 2015, Simmons et al. 2017), and increasingly deep-learning techniques using visually classified training sets (Huertas-Company et al. 2015) as well as unsupervised machine learning (Hocking et al. 2018). Cross-comparisons often show a good concordance between these approaches. This does however not mean that the physical origin of the irregular morphologies, often featuring asymmetries in the form of off-center clumps, can be readily interpreted. While historically frequently used alongside pair counts to quantify the evolution in merger rates, the clumpy morphologies are nowadays more often interpreted as massive star-forming regions originating in marginally stable, gas-rich disks. The tightness of the MS, kinematic evidence for ordered rotation, average surface brightness profiles and axial ratio distributions as well as probes of the cold gas reservoirs all contributed to this paradigm shift. In addition, the wavelength dependence of clumpy morphologies (more prominent in the rest-UV where they are identified) attributed to spatial variations in the SFH and/or dust extinction also imply that the underlying mass distribution is smoother than the galaxies appear in light, unlike what may be expected from mergers (e.g., Wuyts et al. 2012, Cibinel et al. 2015).

Indeed, several studies have addressed the ability to identify mergers at cosmic noon by exploiting mock observations of galaxies extracted from simulated cosmological volumes where their (non-)merger state is intrinsically known (e.g., Snyder et al. 2015, Thompson 2016).
et al. 2015). This exercise reveals dependencies of completeness and contamination fraction of the selected mergers on merger stage, viewing angle, and depth of observation, yielding in some of the simulations that reproduce realistically high gas fractions at $z \sim 2$ results that are no better than a random guess (Abruzzo et al. 2018).

This does not imply that mergers do not happen, nor that all clumps share the same formation process. Targeting mostly higher redshifts ($2 < z < 6$), Ribeiro et al. (2017) find the most massive clumps ($\sim 10^9 M_\odot$) to typically reside in galaxies featuring just 2 clumps, arguably interpretable as a merger, whereas less massive clumps (< $10^9 M_\odot$) occur in galaxies featuring a larger number of them, consistent with disk fragmentation. The distinction between ex-situ and in-situ clumps, with the former featuring higher masses and older stellar ages, is also seen in hydrodynamical simulations (Mandelker et al. 2017).

4.2.2. Clump properties. Turning to the properties of individual clumps, a first realization stemming from multi-band stellar population analyses of these features is that, while striking in appearance, they do not dominate the integrated UV emission of the galaxies, let alone add up to a major contribution of the star formation, and even less so account for a substantial fraction of the overall stellar mass. While a precise breakdown depends on details of sample selection, clump selection (e.g., threshold depth and wavelength), and whether and how underlying diffuse disk emission is accounted for (e.g., Förster Schreiber et al. 2011, Guo et al. 2018), different censuses report clump contributions (i.e., summed over all clumps) to the overall UV emission, SFR, and stellar mass of mass-selected SFGs at cosmic noon of $\sim 20\%$, $\sim 5\%$ – $18\%$ and $\leq 7\%$, respectively (Wuyts et al. 2012, Guo et al. 2015, Soto et al. 2017). The fraction of SFGs that appear clumpy is itself a function of both mass and redshift. While $\sim 60\%$ of low-mass ($\log(M_\star/M_\odot) < 9.8$) SFGs feature clumpy UV morphologies over the full $0.5 < z < 3$ range, the clumpy fraction for intermediate and high-mass SFGs drops from $55\%$ to $40\%$ and from $55\%$ to $15\%$ over the same $z$ range, respectively (Guo et al. 2015).

The characteristic scales of giant star-forming clumps reported in the literature are on the order of a kiloparsec, with corresponding stellar masses ranging up to a few $10^9 M_\odot$ (e.g., Förster Schreiber et al. 2011, Guo et al. 2018). These scales are in accordance with the Toomre scale and mass anticipated for gravitational instabilities within gas-rich turbulent disks (Elmegreen 2009, Genzel et al. 2008, 2011, Dekel et al. 2009a). It is worth noting though that structures on these scales are only marginally resolved in studies of field galaxies, and may correspond to conglomerations of blended clumps of smaller physical scales. Samples of a handful of lensed galaxies reaching spatial resolutions of 20 – 100 pc do indeed reveal progressively smaller clump sizes as the resolution is enhanced with respect to blank field observations (Dessauges-Zavadsky et al. 2017, Rigby et al. 2017). This is illustrated perhaps most convincingly in the analysis of multiple lensed images of the same object at different magnifications (Cava et al. 2018). In this light, zoom-in simulations of turbulent gas-rich disks resolving the multi-phase ISM on parsec scales will prove useful in tracing fragmentation below the Toomre scale and interpreting the higher resolution observations that will become feasible with JWST and ultimately the extremely large telescopes. Already, first attempts on lensed samples are made to characterize the clump mass functions (Dessauges-Zavadsky & Adamo 2018), yielding results consistent with a power-law slope of $-2$ anticipated for fragmentation due to a turbulent cascade (Chandar et al. 2014, Adamo et al. 2017).

Typical stellar ages inferred for the star-forming clumps are on the order of 100 – 200 Myr (Förster Schreiber et al. 2011, Wuyts et al. 2012, Guo et al. 2012, 2018). A single massive clump consisting almost entirely of line emission (i.e., massive in gas, but an order of
magnitude lower in stellar mass) was discovered by Zanella et al. (2015), for which they estimate an age of < 10 Myr, confirming the in-situ formation by gravitational collapse as origin of the clump phenomenon. Mimicking the azimuthally averaged radial trends of stellar population tracers discussed in Section 4.1, clumps themselves also feature redder rest-optical colors, lower Hα EWs, and – inferred from those – older ages (by a few 100 Myr) and lower sSFRs towards the galaxy centers (Förster Schreiber et al. 2011, Adamo et al. 2013, Guo et al. 2012, 2018, Soto et al. 2017). The gradients steepen with increasing stellar mass and decreasing redshift, and are found to be overall steeper than the radial gradients observed for the intra-clump regions (Guo et al. 2018). As a caveat we note that in most of these studies radial gradients are quantified on the basis of ensembles of clumps collected from multiple galaxies within relatively coarse bins of mass and redshift, as the number of detectable clumps in individual systems remains limited.

The longevity of clumps forms an outstanding question with significant implications for the subsequent structural evolution of the galaxies that host them. If remaining intact and surviving internal stellar feedback for a few hundred Myr, their inward migration due to dynamical friction is predicted to be an efficient mode of in-situ bulge growth (e.g., Bournaud et al. 2007, Elmegreen et al. 2008, Ceverino et al. 2010). On the other hand, simulations with stronger feedback implementations such as FIRE (Oklopić et al. 2017) and NIHAO (Buck et al. 2017) feature shorter clump lifetimes (∼ 50 Myr) and substantially less inward migration. Despite their differences both flavors of simulations claim to reproduce the observed phenomenology of wavelength dependent clump prominence, their characteristic stellar ages and even radial gradients (e.g., Oklopić et al. 2017, Mandelker et al. 2014). A duty cycle argument relating the existence of a very young clump as found by Zanella et al. (2015) to the abundance of equally massive clumps that are older supports long inferred clump lifetimes (∼ 500 Myr). Measured ages of the stellar populations in clumps may not necessarily match the timescale of clump survival as clumps are in constant interaction with their surrounding disk due to outflows, tidal stripping, and continued accretion (Bournaud et al. 2014). Perhaps the observable with most discriminating power between the different suites of simulations will prove to be the gas fraction, on an individual clump basis, but even already at the galaxy-integrated level.

4.3. Star-Forming Galaxies as Rotating Turbulent Disks

Near-IR IFU observations, mainly of Hα but also [OIII] or [OII] line emission, have provided the most comprehensive and detailed censuses of the kinematic properties of z ∼ 2 SFGs, and the most convincing evidence for the prevalence of disks among them. Mitigating M/L variations that can complicate the interpretation of morphologies, especially at z > 1, kinematics trace the full underlying mass distribution and are a sensitive probe of a system’s dynamical state. Spatially-resolved kinematics of cold gas line emission from (sub)mm interferometry are still scarce for typical z ∼ 2 MS SFGs, and while near-IR slit spectra have also been exploited to derive emission line kinematic properties, they give spatially limited information with larger uncertainties related to slit placement relative to the galaxy center and kinematic axis. Stellar kinematics at z > 1 are still restricted to quiescent galaxies, absent of young hot stars filling in absorption features, and in all but a few cases are limited to galaxy-integrated velocity dispersions.

The first step in exploiting 3D kinematic data is to identify the nature of the galaxies. Different procedures are followed but they conceptually rely on similar criteria based on
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Rotation curve (RC): Rotation velocity \( v \) vs. galactocentric radius \( r \). For a “Freeman” thin disk with exponential surface density distribution, scale length \( R_d \), and \( y \equiv r/2R_d \), \( v^2(r) = 4\pi G \Sigma_0 R_d y^2 [J_0(y)K_0(y) - I_1(y)K_1(y)] \), where \( G \) is the gravitational constant, \( \Sigma_0 \) is the central surface density, and \( I_i \) and \( K_i \) are the modified Bessel functions of order \( i \). At fixed mass profile \( M(r) \), thick disks (scale height \( h \sim 0.2 - 0.3 R_d \)) have a \( \sim 8\% \) lower \( v \) peak reached at \( \sim 10\% \) larger radius, while in the spherical approximation the peak is \( \sim 15\% \) lower and at \( \sim 20\% \) smaller radius (Freeman 1970, Binney & Tremaine 2008, Noordermeer 2008).

\( v_{\text{rot}} \): Maximum intrinsic rotation velocity (i.e., corrected for beam smearing and galaxy inclination when measured from observations), with \( R_{\text{max}} \) denoting the radius where it is reached in intrinsic space.

\( v_{2.2} \): Intrinsic rotation velocity at \( r = 2.2 R_d \), where a Freeman disk RC peaks (corresponding to 1.3 \( R_e \)). For \( n \neq 1 \) profiles, \( v_{2.2} \) differs from the peak \( v_{\text{rot}} \).

\( \sigma_0 \): Local intrinsic velocity dispersion (i.e., corrected for beam smearing when derived from observations); it is assumed to be isotropic and constant across disks (Section 4.3.2).

\( v_c \): Circular velocity, here as a measure of the potential well. For a thin disk, \( v_c = v_{\text{rot}} \); for a thick disk with non-negligible turbulent pressure gradient, \( v_c^2(r) = v_{\text{rot}}^2(r) + 2 \sigma_0^2 (r/R_d) \) (e.g., Burkert et al. 2016).

\( S_{0.5} \): Alternative kinematic estimator for a spherically symmetric system in an isothermal potential, defined as \( S_{0.5}^2 = 0.5 v_{\text{rot}}^2 + \sigma_0^2 \) (e.g. Weiner et al. 2006a).

\( M_{\text{dyn}} \): Enclosed dynamical mass. For a spherical distribution, \( M_{\text{dyn}}(r) = r v_c^2 / G \); for a Freeman disk, \( M_{\text{dyn}}(r) = 2\pi \Sigma_0 R_d^2 [1 - e^{-r/R_d}(1 + r/R_d)] \) (Binney & Tremaine 2008).

\( \mathcal{f}_s, \mathcal{f}_{\text{bar}}, \mathcal{f}_{\text{DM}} \): Ratio of stellar, baryonic, and DM mass to dynamical mass.

\( j_d \): Specific angular momentum of a (disk) galaxy, \( \propto v(r) \times r \).

2D maps, and on the main derived parameters of maximum rotation velocity \( v_{\text{rot}} \) and local velocity dispersion \( \sigma_0 \) corrected as appropriate for spatial and spectral resolution and for galaxy inclination (extraction methods are summarized in the Supplemental Text). The basis is encapsulated in the following set of disk criteria adopted in several studies, motivated by expectations for an ideal rotating disk, and increasingly stringent and demanding of the data (e.g., Förster Schreiber et al. 2018, Wisnioski et al. 2019):

1. a smooth monotonic velocity gradient across the galaxy, defining the kinematic axis;
2. a centrally peaked velocity dispersion distribution with maximum at the position of steepest velocity gradient, defining the kinematic center;
3. dominant rotational support, quantified by the \( v_{\text{rot}} / \sigma_0 \) ratio;
4. co-aligned morphological and kinematic major axes (a.k.a. kinematic misalignment);
5. spatial coincidence of the kinematic and morphological centers.

Application of these criteria is usually done from measurements of the parameters and visual inspection, or through comparisons to disk models. Kinemetry, an approach based on harmonic expansion along ellipses of the moment maps of the line-of-sight velocity distribution, has also been used in some studies to quantify the degree of asymmetry in velocity and dispersion maps, either as main classification or in support of the criteria above. Details on disk modeling and kinemetry can be found in the Supplemental Text. It is increasingly common to supplement the kinematic criteria with information on galaxy morphology and possible companions, e.g., from HST imaging, for a more complete characterization.
The outcome of the morpho-kinematic classification scheme depends on how well the galaxies are resolved and how sensitive the data are. It is usually adequate to provide a first-order description of the system and the basis for quantitative interpretation of the measurements. Deeper data detecting fainter extended emission and/or higher resolution (AO-assisted vs. seeing-limited) set better constraints on the nature of the galaxies and can reveal additional interesting features (Section 4.5). The choice of $v_{\text{rot}}/\sigma_0$ threshold varies from 1 to 3 between different studies, with the intermediate value of $\sqrt{3.36}$ corresponding to equal contribution from rotation and random motions to the dynamical support of a turbulent disk. Several efforts have been devoted to assess the reliability of kinematic classification based on mock observations of template data, encompassing nearby systems to high resolution cosmological simulations. Low misclassification fractions of $\sim 10\% - 30\%$ are generally obtained for disks and major mergers alike, with the range reflecting the specific criteria employed, and data resolution and S/N (Shapiro et al. 2008, Epinat et al. 2010). Using zoom-in simulations from the VELA suite of $z \sim 2$ isolated galaxies and mergers over many sightlines to create $\sim 24000$ mock-observed data sets in $0.6''$ seeing, Simons et al. (2019) conclude that disks are identified with high confidence, while misclassification of mergers as disks varies widely but, unsurprisingly, is lowest ($\sim < 20\%$) when applying all criteria above and folding in HST-like morphological information.

4.3.1. Disk fractions. Recent large kinematic surveys have confirmed the findings from earlier smaller samples that up to $z \sim 2.5$ a large proportion of massive SFGs are fairly regular disks, albeit with higher velocity dispersions than present-day spirals. The largest and most complete surveys, comprising hundreds of SFGs on/around the MS at $9 \lesssim \log(M_*/M_\odot) \lesssim 11.5$ with resolved kinematics from KMOS, find $\sim 70\% - 80\%$ of rotation-dominated galaxies (i.e., satisfying criteria 1-3 above, with $v_{\text{rot}}/\sigma_0 > 1$; Wisnioski et al. 2015, 2019, Stott et al. 2016), a result borne out by deep AO-assisted SINFONI data of $35 z \sim 1.5 - 2.5$ SFGs in the same mass range (Förster Schreiber et al. 2018). Imposing all criteria reduces the disk fractions $f_{\text{disk}}$ to $\sim 50\% - 60\%$. Significant trends in the kinematic mix of SFGs are emerging from $z \gtrsim 0.6$ IFU surveys, with lower $f_{\text{disk}}$ at earlier epochs and, at fixed $z$, towards lower masses (e.g., Wisnioski et al. 2019, Turner et al. 2017). These results strengthen and extend out to $z \sim 3.5$ findings from optical and near-IR slit spectroscopy over $z \sim 0.2 - 2.5$ (e.g., Kassin et al. 2012, Simons et al. 2017). The dependence on $M_*$ and $z$ of the fraction of rotation-dominated galaxies is illustrated in Figure 4 (where the curves are adjusted to match the binned data presented by Simons et al. 2017, Turner et al. 2017, and Wisnioski et al. 2019). The trends reflect primarily those with $v_{\text{rot}}/\sigma_0$, with the evolution of $\sigma_0$ largely driving the $z$ variation and the connection between $v_{\text{rot}}$ and galaxy mass (via the Tully-Fisher relation) dominating the $M_*$ dependence (see Sections 4.3.2 and 4.4.2). They also account for the range in $f_{\text{disk}}$ ($\sim 25\% - 75\%$) reported by various $z \sim 0.5 - 3.5$ studies based on samples of $\sim 10 - 60$ SFGs probing different mass and redshift ranges, in addition to other factors such as S/N, resolution, details and strictness of the classification procedure (e.g., Law et al. 2009, Epinat et al. 2012, Livermore et al. 2015, Mieda et al. 2016, Mason et al. 2017, Girard et al. 2018a, Gillman et al. 2019).

The variation of disk fraction and $v_{\text{rot}}/\sigma_0$ with galaxy mass and redshift has been

\[f_{\text{disk}}: \text{Fraction of galaxies classified as disks.}\]
interpreted in a “disk settling” scenario (Kassin et al. 2012). Massive SFGs settled earlier into more rotationally-dominated “mature” disks, gradually followed by lower-mass galaxies at later times and with more massive disks being dynamically colder at all epochs. This evolution is reflected in the trends between mass, morphology, and specific angular momentum of disks (discussed in Section 4.4.4). It also finds its counterpart in the structure of the stellar component from HST imaging inferred from the projected axial ratio distributions (Section 4.2), and is qualitatively reproduced by the recent high-resolution TNG50 cosmological simulation (Pillepich et al. 2019).

Sections 4.3.2 and 4.4 focus on the properties of disks identified as described above and interpreted in an ideal disk framework, Section 4.5 comments on deviations thereof. The mass dependence of the disk fraction implies that disk samples preferentially probe, on average, higher mass SFGs compared to mass-selected samples.

### 4.3.2. Disk turbulence.

The elevated gas velocity dispersion of $z \sim 2$ disks is well established and implies that they are geometrically thick as observed in HST imaging (e.g., Elmegreen & Elmegreen 2003, 2017). At the level of beam smearing of high-$z$ observations ($\sim 4 - 5$ kpc in natural seeing, and $\sim 1 - 2$ kpc using AO), unresolved noncircular motions induced by deviations from axisymmetry of the gravitational potential (e.g., massive clumps, bars) or related to outflows may contribute to the measured $\sigma_0$ along with local turbulent gas motions. The agreement in $\sigma_0$ between no-AO and AO data sets (after beam smearing corrections) suggests that potential noncircular motions on $\gtrsim 1$ kpc scales have little impact on the measurements. For simplicity, $\sigma_0$ is usually referred to as “turbulence.”

Typical dispersions measured in ionized gas are $\sim 45$ km s$^{-1}$ at $z \sim 2$, compared to $\sim 25$ km s$^{-1}$ at $z \sim 0$, varying as $\sigma_0 \approx 23 + 10z$ km s$^{-1}$; cold atomic and molecular gas measurements at $z > 0$ are scarcer but follow a similar evolution albeit with $\sim 10 - 15$ km s$^{-1}$ lower dispersions (Übler et al. 2019 and references therein). The $\sigma_0$ evolution is consistent with that of the galactic gas mass fractions in the framework of marginally-stable $Q \sim 1$ gas-rich disks in which $v_{rot}/\sigma_0 \propto f_{gas}^{-1}$ (e.g., Genzel et al. 2011, Wisnioski et al. 2015, Johnson et al. 2018). At fixed redshift, the scatter in $\sigma_0$ is substantial and there is evidence that an important part of it is intrinsic to the galaxy population, but only a weak or no trend is found between $\sigma_0$ and global galaxy parameters such as $M_*$, SFR, $f_{gas}$, mass and SFR surface densities, or inclination (e.g., Jones et al. 2010a, Genzel et al. 2011, Johnson et al. 2018, Übler et al. 2019). Reasons could include limited ranges and uncertainties in properties in a given $z$ slice, complex dependence of $\sigma_0$ on more than one parameter, or possible accretion-driven variations on short $\lesssim 100$ Myr timescales as recently proposed by Hung et al. (2019) based on FIRE high-resolution numerical simulations. In high S/N AO data of well resolved disks, no convincing trend on spatially-resolved $\sim 1 - 2$ kpc scales has been seen either between $\sigma_0$, $\Sigma_{SFR}$, or even galactocentric radius in the outer disk parts (away from where beam smearing corrections become large and more uncertain; Förster Schreiber et al. 2018, Übler et al. 2019). Given the lack of clear variations, the disk dispersions are thus taken as isotropic and radially constant.

Constraining the physical driver(s) of the gas turbulence at high $z$ thus still proves difficult. This supersonic turbulence would rapidly decay within a crossing time ($\sim 10^7$ yr)

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6For a disk of finite intrinsic thickness $q_0 = (b/a)_0$, the inclination $i$ is obtained via $\sin^2(i) = (1 - q_0^2)/(1 - q_0^2)$; for $q_0 \sim 0.2$ suggested by axial ratio (and $v_{rot}/\sigma_0$) distributions at $z \sim 2$, the difference in inclination correction compared to $q_0 = 0$ amounts to $\sim 2\%$ or less.
if not continuously powered, and gas accretion from the cosmic web, disk instabilities, and stellar feedback have been proposed as energy sources (see, e.g., summaries by Krumholz et al. 2018, Übler et al. 2019). Theoretical models and numerical simulations make different predictions as to the generated amount of gas turbulence (e.g., Aumer et al. 2010, Hopkins et al. 2012, Gatto et al. 2015, Goldbaum et al. 2015, 2016). The impact of stellar feedback varies a lot depending on the inclusion/treatment of radiation pressure and the location where feedback is injected into the ISM, although a general conclusion is that it can maintain galaxy-wide turbulence of $\sim 10^{-20}$ km s$^{-1}$ (and is necessary to reproduce various other galaxy properties and scaling relations). In contrast, gravitational processes including gas transport and instabilities within the disks appear to more easily match the observed range of $\sigma_0$ under the conditions prevailing at higher redshifts. Plausibly, both forms of drivers are present as in the unified model of Krumholz et al. (2018), with gravity-driving dominating at earlier cosmic times and a gradual transition to feedback-driving at later times. Further insights will benefit from more direct estimates of cold gas masses in individual galaxies, and maps of the gas, SFR, and kinematics at high spatial and velocity resolution.

4.4. Mass and Angular Momentum Budget

Constraints from resolved kinematics have been used to investigate the mass budget and angular momentum of high $z$ SFGs. At $z \sim 2$, it is important to account for the significant contribution of gas to the baryonic component, and of the random motions to the dynamical support. In the turbulent disk framework, the circular velocity $v_c$ (as a measure of the potential well) at radius $r$ can be computed through $v_c^2 = v_{\text{rot}}^2 + 2\sigma_0^2 (r/R_d)$. Corrections can be applied for deviations from $n \approx 1$ profiles (e.g., when a massive bulge is present), and for disk “truncation” appreciably reducing $R_e/R_d$ in strongly dispersion-dominated cases $v_{\text{rot}}/\sigma_0 \lesssim 2$ (Burkert et al. 2016). The enclosed dynamical mass can be estimated, for instance at $R_e$, through $M_{\text{dyn}} = R_e v_c^2 / G$, where $G$ is the gravitational constant. This expression is for the spherical approximation; for an infinitely thin Freeman disk the values would scale down by $\times 0.8$. Other methods to derive dynamical masses have been used, including a two-pronged approach applying the rotating disk estimator neglecting pressure support for rotation-dominated disks (i.e., taking $v_c = v_{\text{rot}}$) and through the virial mass estimator with the integrated dispersion for dispersion-dominated sources ($M_{\text{dyn}} = \alpha R_e \sigma^2 / G$ with $\alpha$ in the range $\sim 3 - 5$ typically adopted). Forward modeling accounting for disk thickness and turbulence, and fitting simultaneously the velocity and dispersion profiles, incorporates self-consistently all relevant effects though comparisons with simpler approaches as outlined above indicate overall agreement within $\sim 0.2$ dex (e.g., Förster Schreiber et al. 2018).

4.4.1. Dynamical vs. baryonic mass estimates. In the most straightforward approach to constraining the mass budget, global dynamical mass estimates are compared to stellar and gas mass estimates. Studies based on near-IR IFU or slit spectroscopy data generally concur on overall elevated baryonic mass fractions $f_{\text{bar}} = (M_* + M_{\text{gas}}) / M_{\text{dyn}}$, with large scatter, among $z \sim 2$ SFGs (e.g., Förster Schreiber et al. 2009, Stott et al. 2016, Price et al. 2020). Modeling deep H$\alpha$ kinematic data over a wide $M_*$ range across $z \sim 0.7 - 2.7$ from the KMOS3D survey in legacy fields providing detailed constraints on galaxy stellar and size properties, Wuyts et al. (2016b) found a large rise in $f_{\text{bar}}$ derived within the central 1 $R_e$ regions from $\sim 45\%$ at $z \sim 0.9$ to $\sim 90\%$ at $z \sim 2.3$ and a modest increase in stellar mass fraction $f_\ast = M_\ast / M_{\text{dyn}}$ from $\sim 30\%$ to $\sim 40\%$, reflecting the $f_{\text{gas}}$ evolution. The scatter at
fixed $z$ is driven by positive correlations with average stellar and gas mass surface densities at $< R_e$. These trends hold when accounting for mass incompleteness or considering only progenitors of $z = 0 \log(M_*/M_\odot) \geq 10.7$ galaxies, and are fairly robust to SED modeling assumptions or gas scaling relations among plausible choices. At $z \sim 2$, the $M_{\text{dyn}}$-based results thus leave little room for DM mass contribution ($f_{\text{DM}}$) within the $\sim 1 - 2 R_e$ probed by the observations. Noting that the analyses above are for a Chabrier IMF, more bottom-heavy galaxy-wide IMFs such as a Salpeter slope down to 0.1 $M_\odot$ would also be disfavored.

**4.4.2. Tully-Fisher relation.** The Tully-Fisher relation (TFR) relates measures of galaxy mass to the full potential well; it is thus sensitive to the galactic baryonic content and can place powerful constraints on cosmological disk formation models (e.g., [Mo et al. 1998], [Dutton et al. 2007], [Somerville et al. 2008], [McGaugh 2012], among many others). Kinematic studies agree on the existence of a TFR out to $z \sim 3$ and on the reduced scatter about the relation when accounting for pressure support in the turbulent high $z$ disks but with mixed outcome as to the evolution, ranging from none over $z \sim 0 - 1$ (e.g., [Kassin et al. 2007], [Miller et al. 2012], [Tiley et al. 2019a]) to significant in the sense of lower disk mass at fixed velocity for $z \sim 0.6 - 3.5$ samples (e.g., [Cresci et al. 2009], [Turner et al. 2017], [¨Ubler et al. 2017]). The conclusions hinge on several interrelated factors including the adopted form and parametrization of the relation, galaxy sample properties, and choice of reference $z \sim 0$ TFR ([¨Ubler et al. 2017], [Tiley et al. 2019a]). The range in galaxy parameters spanned by the high $z$ data sets generally hampers reliable fits to the slope of the relation, such that the evolution is usually quantified in terms of the zero-point (ZP) obtained assuming a non-evolving slope. The magnitude of the ZP offsets also depends on whether the relation is constructed from the stellar or the baryonic mass, and from $v_{\text{rot}}$, $v_{2.2}$, $v_c$, or $S_{0.5}$.

Exploiting the wide $0.7 < z < 2.7$ baseline from KMOS3D, the study of [¨Ubler et al. 2017] provided the most self-consistent constraints across cosmic noon based on H$_\alpha$ kinematics from IFU observations, identical analysis method, selection through uniform data quality, galaxy parameters, and stringent disk criteria, with resulting log($M_*/M_\odot$) > 10 subsamples well matched in $M_*$ and location around the MS and mass-size relations. Focussing on (fixed-slope) relations in terms of $v_c$, the stellar TFR shows no significant ZP evolution from $z \sim 2.3$ to $0.9$ while the baryonic TFR ZP exhibits a negative evolution (lower $M_{\text{bat}}$ at fixed $v_c$), and both relations imply similar positive evolution since $z \sim 0.9$ compared to published $z \sim 0$ TFRs. In the latter redshift interval, [Tiley et al. 2019a] found instead little, if any, evolution in terms of $M_* - v_{2.2}$ using matched data quality, methods, and samples over log($M_*/M_\odot$) $\sim 9 - 11$ from the KROSS and local SAMI IFU surveys of H$_\alpha$. The persisting discrepancies around $z \sim 1$ underscore the importance of disentangling observationally- and physically-driven effects in order to establish firmly the evolution and explore the residuals of the TFR across all of $0 < z < 3$.

**4.4.3. Outer disk rotation curves.** Constraining the mass distribution from the shape of the rotation curve (RC) alleviates the uncertainties of global M/L conversions for the baryonic components. This approach is challenging at $z \sim 2$ with current instrumentation, as tracing emission line kinematics beyond $\sim 1 - 2 R_e$ requires very long integrations.

Recent results from very sensitive H$_\alpha$ IFU data of a handful of massive $z \sim 1 - 2.5$ star-forming disks extending to $r \sim 10 - 20$ kpc showed significant and symmetric drops in the individual RCs beyond their peak ([Genzel et al. 2017]). Similar falloffs in stacked H$_\alpha$ RCs reaching $\sim 3.5 - 4 R_e$ constructed from high quality IFU data of $\sim 100$ typical
Example kinematic modeling of a massive $z=1.4$ SFG with sensitive Hα and CO 3-2 observations, a bulge-to-total mass ratio of $\sim 0.25$, and large $v_{\text{rot}}/\sigma_0 \sim 10$ (from Ubler et al. 2018). Left: RC in observed and intrinsic space. The observed, folded Hα and CO velocity curve (grey squares) extends to 18 kpc. The best-fit model curve of the circular velocity ($v_c$) in intrinsic space is plotted as blue line (with blue shading showing the 1σ uncertainties of the inclination correction). The other lines show, successively, the effects of pressure support (i.e., the $v_{\text{rot}}$ curve; cyan line) that are minimal in this galaxy, the effects of inclination ($v_{\text{rot}} \times \sin(i)$; yellow line), and the resulting beam-smeared velocity curve in observed space (red line). Right: The relative contribution to the model $v_c$ in intrinsic space (blue line) from the baryons and from the DM halo (green and purple lines, respectively). Baryons strongly dominate within the half-light radius while DM starts to dominate the mass budget beyond $\approx 12$ kpc or $\approx 3R_e$ (vertical solid and dashed lines).

log($M_\star/M_\odot$) $\gtrsim 10$ star-forming disks suggested that this behaviour may be widespread at high $z$, and on average more pronounced towards higher $z$ and lower $v_{\text{rot}}/\sigma_0$ disks (Lang et al. 2017). The outer slopes for these samples are nearly Keplerian, and in stark contrast to the flat or rising RCs of local spirals. The falloffs can be naturally explained as the imprint of baryons strongly dominating the mass over the regions probed by the kinematics together with sizeable levels of pressure support maintained well past the RC peak. The more detailed constraints from the individual extended RCs and dispersion profiles, simultaneously fit with turbulent disk + bulge + DM halo models, yield $f_{\text{DM}}(R_e) \lesssim 20\%$ with the 3/6 galaxies at $z > 2$ having the lowest fractions. In turn, the stacked RC is best matched by models with a high fraction of total baryonic disk mass to DM halo mass $m_d \sim 0.05$, in line with analysis of the angular momenta of a larger sample of $z \sim 0.8 – 2.6$ SFGs (Burkert et al. 2016) and consistent with abundance matching results once accounting for the high $f_{\text{gas}}$ at high $z$ ($M_\star/M_{\text{halo}} \sim 0.02$; Moster et al. 2013, Behroozi et al. 2013a). Although the exact numbers depend on details of the distribution of the mass components, the implications of low central DM fractions and an overall high disk to DM halo mass ratio were shown to be fairly robust to the assumptions within plausible ranges.

These findings spurred a number of follow-up studies, reporting mixed results. For instance, Tiley et al. (2019b) concluded that the averaged Hα outer RCs at $z \sim 0.9 – 2.5$ are flat or rising, in contrast to Lang et al. (2017). As noted by both groups, stacking methodology matters. Re-scaling the data according to the observed radius $R_{\text{max}}$ and velocity at
Figure 7
Location of 40 massive $z \sim 0.7 - 2.7$ SFGs in a diagram of the baryonic mass vs. inner ($< R_e$) DM mass fraction. The $f_{\text{DM}}(R_e)$ is derived from kinematic modeling (as shown in Figure 6) of high quality Hα and CO RCs (and velocity dispersion profiles) extending out to radii in the range $10 - 20$ kpc from the samples of Genzel et al. (2017, 2020) and Übler et al. (2018) (red and blue circles for $z \sim 2$ and $z \sim 1$ disks), with typical uncertainties of $\pm 0.1 - 0.15$ for individual $f_{\text{DM}}(R_e)$ estimates. Median $f_{\text{DM}}(R_e)$ from modeling the inner regions kinematics of larger SFG samples at $z \sim 2.3$ (red square) and $z \sim 0.9$ (blue square) from Wuyts et al. (2016b) are overplotted, as well as results from quiescent galaxies at $z \sim 1.7$ based on stellar velocity dispersions presented by Mendel et al. (2020). Approximate areas occupied by $z = 0$ massive early-type and late-type galaxies (ETGs, LTGs; from Cappellari et al. 2013 and Martinsson et al. 2013) and the Milky Way (Bland-Hawthorn & Gerhard 2016) are indicated with blue shading and the cross-hair symbol.

the RC peak as favored by Lang et al. is more sensitive to the relative concentration of baryons vs. DM and, although it relies on detecting a change of slope in the inner velocity gradient, possible biases against recovery of flat or rising RCs were shown to be unlikely. Normalizing instead with the radius and velocity in observed space corresponding to $3 R_d$ based on $n = 1$ fits to the morphologies as favored by Tiley et al. probes the baryonic to DM content on more global scales but any spread in $R_{\text{max}}/R_d$ from a range in Sérsic indices would smear the peak in the composite RC. Importantly, the stacked samples are different, with the Lang et al. stricter disk selection resulting in higher mass and $v_{\text{rot}}/\sigma_0$ ranges compared to Tiley et al. Comparisons are therefore not straightforward but given the large variations in $f_{\text{DM}}$ with radius, the conclusion of Tiley et al. (2019b) that within $6 R_d \approx 3.6 R_e$ high $z$ SFGs are DM-dominated is not necessarily incompatible with them being strongly baryon-dominated within $1 R_e$, even when displaying a flat outer RC in high $v_{\text{rot}}/\sigma_0$ cases (Figure 6 and, e.g., Übler et al. 2018). On-going extensions to several tens
of $z \sim 0.7 - 2.7$ disks with high quality individual kinematics data are revealing ever more clearly a dependence with galaxy mass, redshift, and measures of central baryonic mass concentration (Genzel et al. 2020), which were apparent in some previous outer RC studies. These trends echo the findings from the global mass budget (Section 4.4.1), account for the strong baryon dominance to $r \sim 8$ kpc reported by van Dokkum et al. (2015) for 10 compact massive SFGs $2 < z < 2.5$ from the declining composite RC inferred from integrated Hα line widths, and explain the range of conclusions from different outer RC samples.

4.4.4. Angular momentum. The connection between $z \sim 2$ SFGs and their host DM halos has been further explored via measurements of the specific angular momentum $j_d \propto v_{\text{rot}} \times R_e$. The inferred halo scale angular momenta are broadly consistent in mean and scatter with the theoretically predicted lognormal distribution of halo spin parameters $\lambda$, and the $j_d$ estimates scale approximately as $\propto M^{2/3}_{DM}$ (e.g., Burkert et al. 2016, Harrison et al. 2017, Swinbank et al. 2017). The long made assumption that on average $j_d/j_{DM} \sim 1$, expected if disks retain most of the specific angular momentum acquired by tidal torques in their early formation phases and shown to hold for local spirals (e.g., Fall & Romanowsky 2013), thus appears to be borne out by observations up to $z \sim 2.5$. Even in a population-wide sense, this finding is not trivial given that (i) infalling baryons can lose and gain angular momentum from the virial to the disk scale (e.g., Danovich et al. 2015), (ii) angular momentum can be efficiently redistributed in and out of galaxies (e.g., Dekel et al. 2009a, Ubler et al. 2014, Bournaud 2016), and (iii) < 15% of the cosmically available baryons are incorporated into the stellar component of galaxies ($m_1, \approx 0.02$; e.g., Moster et al. 2013, Behroozi et al. 2013a) and at most 30% when including gas at $z \sim 2$ (Burkert et al. 2016). Although simulations and semi-analytical models are now able to produce realistic distributions of galaxy size, specific angular momentum, and stellar-to-halo mass ratios, there is no consensus yet on how various mechanisms interact to preserve net angular momentum (e.g., Genel et al. 2015, Zavala et al. 2016, Jiang et al. 2019).

The observed scatter in specific angular momenta has an intrinsic component at all epochs. The low $j_d$ tail encompasses massive early-type spirals and ellipticals at $z \sim 0$, and more dispersion-dominated (and unstable) as well as more centrally concentrated star-forming disks in the high $z$ samples. These correlations reflect an underlying mass-spin-morphology relation that likely underpins the Hubble sequence (e.g., Obreschkow & Glazebrook 2014) and may suggest that “disk settling” with cosmic time (see Section 4.3) is driven at least in part by angular momentum evolution (e.g., Swinbank et al. 2017). Noting that central mass concentration increases with galaxy mass and thus “disk maturity” (see Sections 4.1 and 4.3), Burkert et al. (2016) found in their $z \sim 0.7 - 2.6$ sample of star-forming disks a significantly weaker anticorrelation between $\lambda \times (j_d/j_{DM})$ and central stellar surface density $\Sigma_{1kpc}$ than with the galaxy-averaged $\Sigma_*$ and $\Sigma_{gas}$ – a result suggesting that accumulation of (low angular momentum) material in the galaxy centers may be decoupled from the processes that set the global disk scale and angular momentum.

4.4.5. Interpreting the mass and angular momentum budget. A consistent picture appears to be emerging in which log($M_\star/M_\odot$) $\gtrsim 10$ star-forming disks at $z \sim 2$ are typically baryon-rich on the physical scales probed by the data, with lower DM mass contribution at $< 1R_e$ among more massive, centrally denser, and higher $z$ galaxies. These trends are qualitatively reproduced by matched populations (in $M_\star$, SFR, $R_e$) in recent cosmological numerical simulations (e.g., Wuyts et al. 2016b, Swinbank et al. 2017, Lovell et al. 2018).
While the role of the evolving gas content can be easily understood, the trends in mass fractions and ZP of the TFRs point to differences in the relative distribution of baryons vs. DM on galactic scales among SFGs of comparable masses at different cosmic epochs. These have been ascribed to a combination of (i) disk size growth at fixed mass, where the baryons at lower z extend further into the surrounding DM halo, (ii) evolving DM halo profiles, with shallower inner profiles at earlier times (e.g., less concentrated, or more cored; Martizzi et al. 2012 Dutton & Macciò 2014), and (iii) efficient dissipative processes in the gas-rich environments at higher z concentrating baryons in the central regions (e.g., Dekel & Burkert 2014 Zolotov et al. 2015). The weaker coupling between $\lambda \times (j_{\text{d}}/j_{\text{DM}})$ and $\Sigma_{1\text{kpc}}$ vs. $\Sigma_{\text{gas}}$ (Burkert et al. 2016) would naturally result from inward radial gas transport through the latter processes.

The kinematically inferred low $f_{\text{DM}}(R_e)$ of massive $z \sim 2$ star-forming disks overlaps with the range for $z \sim 0$ massive early-type galaxies — their likely descendants. This echoes evolutionary links based, for instance, on the stellar sizes and central mass densities (Section 3.4 and 4.1), and on the fossil record (e.g., Cappellari 2016). Current $z \sim 2$ results are summarized in Figure 7 (following Genzel et al. 2017 Ubler et al. 2018) incorporating an expanded sample of individually modeled RCs (Genzel et al. 2020). The inverse dependence of $f_{\text{DM}}(R_e)$ with galaxy mass (and mass concentration) is reminiscent of the trends observed in local disks captured by the unified picture of Courteau & Dutton (2015). In this picture, the outward moving transition from baryon-dominated center to DM-dominated outskirts (relative to a fiducial $2.2 R_d \approx 1.3 R_e$ for $n \sim 1$) in more massive systems can be tied to the disk size – circular velocity – stellar mass scaling relations, with scatter in $f_{\text{DM}}$ attributed at least in part to size variations at fixed $v_c$. The differentiation in $f_{\text{DM}}(R_e)$ at fixed mass seen between local early- and late-type galaxies (e.g., Courteau & Dutton 2015) also appears to be present at cosmic noon (e.g., Mendel et al. 2020), which plausibly is rooted in the same processes that lead to the distinction between SFGs and quiescent galaxies in their stellar structural properties (e.g., Lang et al. 2014 van der Wel et al. 2014a).

By necessity, the kinematics of $z \sim 2$ star-forming disks are interpreted in a simplified axisymmetric framework with circular orbital motions. Observations of local disks indicate frequent deviations from this simple assumption caused, for instance, by interactions, warps and other such dynamical instabilities, and radial motions, which are difficult to constrain at the typical resolution and S/N of high-$z$ data. Signatures of the latter are discussed in the next Section. Bending instabilities, such as warping or buckling, may be expected to be suppressed or short-lived in gas-rich turbulent disks (see the discussion by Genzel et al. 2017). Minor interaction-induced perturbations may not be ruled out but the exclusion of galaxies with potential companions wherever possible should reduce their role in disk samples. The validity of the disk framework for low-mass objects may be called into question in light of the increasing prevalence of prolate and/or triaxial systems towards lower masses and higher $z$ suggested by statistical studies of the morphological axial ratios (Section 4.2), although this may be a lesser concern when applying the morpho-kinematic disk criteria (notably the requirement of kinematic and morphological major axes alignment; e.g., Franx et al. 1991). Furthermore, the generally small and spatially flat residuals in velocity and dispersion maps compared to axisymmetric disk models (resulting from the disk selection criteria employed in most studies) suggest that the potential impact of minor merger perturbations and prolateness/triaxiality is small in the kinematic analyses.

Cosmological simulations are useful to assess the validity of assumptions made in interpreting data under more realistic high redshift environments. For instance, Wellons et al. 2020.
quantified the effects of pressure gradients, noncircular motions, and asphericity in the gravitational potential on the rotation velocity and $M_{\text{dyn}}$ estimates in high-resolution FIRE numerical simulations of a range of massive turbulent disks at $1 \lesssim z \lesssim 3$ based on the mass particle distributions, finding that pressure support usually makes the largest impact and that when it is accounted for, kinematically-derived mass profiles agree with the true enclosed mass within $\sim 10\%$ typically over the $r \lesssim 10 - 20$ kpc range explored. Realistically replicating observables and empirical methodologies from simulations is not straightforward and subject to various limitations (numerical resolution, sub-grid recipes, radiative transfer, ... ) but the informative potential is motivating a growing number of investigations to improve on both the simulation ingredients and data interpretation.

4.5. Deviations from Disk Rotation

In kinematics data of $z \sim 2$ SFGs, modest deviations from regular patterns are seen in a subset of galaxies otherwise consistent with global disk rotation. Interpreting such kinematic asymmetries is not trivial in high $z$ data but can plausibly be ascribed to internally- or externally-induced in-disk inflows, or to outflows. As will be discussed further in the next Section, the emission associated with the latter has a broad velocity distribution but low amplitude, and should have a negligible effect on the single-component line profile fitting that is usually performed in extracting 2D kinematic maps, unless the outflow is particularly strong (Förster Schreiber et al. 2018). The gas-rich environments prevailing at $z \sim 2$ are expected to naturally promote perturbations in the marginally-stable $Q \sim 1$ gas-rich disks, with fragmentation and efficient transport of material towards the center via, e.g., inward gas streaming and clump migration, while the gas reservoirs of galaxies are continuously replenished by anisotropic accretion via streams and minor mergers. Material streaming inwards can induce twists in the isovelocity contours and off-center peaks in the dispersion map at the level of a few tens of km s$^{-1}$ ($v_{\text{rad}} \sim 2 \times \sigma_0 \times (\sigma_0/v_{\text{rot}})$), and differences in magnitude and orientation of the angular momentum between inner and outer regions expected to remain even after bulge growth slows (e.g., van der Kruit & Allen 1978, Cappellari 2016). Characteristic signatures thereof are indeed identified in some of the $z \sim 2$ galaxies with high S/N, high resolution AO-assisted observations, along with morphologically identified bar- and spiral-like features in some cases (e.g., Genzel et al. 2006, Law et al. 2012a, Förster Schreiber et al. 2018). These processes may be important in bulge and SMBH buildup, and concurrent disk growth through angular momentum redistribution (e.g., Bournaud et al. 2014, Dekel & Burkert 2014, Zolotov et al. 2015). The ubiquity of dense stellar cores and large nuclear concentrations of cold gas in massive $z \sim 2$ SFGs, and the weak correlation between disk-scale angular momentum with $\Sigma_{1\text{kpc}}$ call for further sensitive and high resolution kinematics data to more directly assess the role of radial gas transport at cosmic noon vs. alternative scenarios such as inside-out galaxy growth (van Dokkum et al. 2015, Lilly & Carollo 2016).

Strong kinematic distortions are generally interpreted as indicative of major merging. Assuming very simplistically that all SFGs not identified as rotation-dominated disks according to the classification scheme of Section 4.3 are major mergers, the fractions thereof would be $\sim 25\% - 40\%$ at $z \sim 1 - 2.5$ and $\log(M_*/M_\odot) \gtrsim 10.5$ (depending on the exact
set of criteria and $z$ [Wisnioski et al. 2019]. These fractions are comparable to those inferred from morphologies and close pair statistics in a similar mass range (e.g., Conselice 2014, López-Sanjuan et al. 2013, Rodrigues et al. 2018), and consistent with cosmological simulations (e.g., Genel et al. 2008, Snyder et al. 2017). Taking the major merger fraction as $1 - f_{\text{disk}}$ is obviously an oversimplification. Shallower data are more biased towards high surface brightness regions that may partly and unevenly sample the full system and result in apparently disturbed kinematics, exacerbated for clumpy morphologies (see Fig. 9 of Förster Schreiber et al. 2018). A poorly resolved, low $v_{\text{rot}}/\sigma_0$ object does not necessarily imply it is a major merger [Newman et al. 2013]. More face-on disks may also be more difficult to identify because of the resulting small projected velocity gradient, reduced central dispersion peak, and possible clumps biasing the determination of morphological position angle and center [Wuyts et al. 2016b]. As is the case for morphologies, kinematic signatures of interactions depend strongly on the system’s orbital configuration, the properties and mass ratio of the progenitor galaxies, the sightline, and the merger stage (e.g., Bellocchi et al. 2016, Simons et al. 2019), introducing uncertainties in identifying major mergers. Despite these uncertainties, the kinematic mix among log($M/\text{M}_{\odot}$) $\gtrsim 10$ SFGs at $z \sim 2$ suggests a dominant timescale in a disk configuration, consistent with several other lines of evidence from scaling relations of galaxy properties pointing to the importance of processes other than major merger events in building up stellar mass and structure.

4.6. Galactic-scale Outflows

Galactic winds are thought to play a critical role in the evolution of galaxies by regulating their mass build-up, size growth, star formation, and chemical enrichment, by redistributing angular momentum, and by mediating the relationship between SMBHs and their host galaxies. Stellar feedback at low galaxy masses expels gas from the shallow potential wells, reducing the reservoirs fueling star formation and keeping a low galactic metal content (e.g., Dekel & Silk 1986, Davé et al. 2017). Above the Schechter mass log($M/\text{M}_{\odot}$) $\sim 10.7$ (or log($M_{\text{halo}}/\text{M}_{\odot}$) $\sim 12$), accreting SMBHs are thought to be important in suppressing star formation through ejective “QSO mode” feedback driving powerful winds during high Eddington ratio phases that sweep gas out of the host galaxy, and subsequent preventive “radio mode” feedback maintaining galaxies quenched by depositing kinetic energy into the halo that inhibits cooling alongside virial shocks (see review by Fabian 2012).

Galactic winds should be particularly effective at the peak epoch of star formation and SMBH accretion rates. The most easily accessible diagnostics at high $z$ are rest-UV to optical interstellar (IS) absorption features and nebular emission lines, which probe neutral and warm ionized gas phases. Winds are identified through their kinematic imprint: centroid velocity offsets and broad wings of blueshifted IS absorption relative to the systemic redshift (e.g., from stellar features), redshifted Ly$\alpha$ profile (accessible at $z > 2$), and broad line emission typically underneath a narrower component arising from star-forming regions in the galaxy [8]. Alongside understanding the physical drivers of outflows, a major goal of studies at high $z$ is to assess their role in galaxy evolution. To this aim, population-wide censuses are essential to reveal the global and time-averaged impact of outflows, reducing biases from selection on properties that would be closely linked to the strongest activity.

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8While common, a blueshift for emission line tracers is not necessary; depending on outflow geometry and extinction by dust in the galaxy, backside receding gas can be detected.
Such censuses have been greatly facilitated with the advent of optical and near-IR MOS and IFU instruments. IFU observations have proven particularly powerful, by (i) locating the launching sites and constraining the extent of outflowing gas, and (ii) facilitating the separation between large-scale gravitationally-driven and outflow-related motions that both contribute to velocity broadening in integrated spectra.

4.6.1. Outflow Demographics at \( z \sim 2 \). Much like in the nearby Universe (e.g., Veilleux et al. 2005), SF- and AGN-driven winds at high \( z \) are distinguished on the basis of their velocities, spatial origin, and excitation properties (Figure 5). SF-driven outflows with velocities up to several 100 km s\(^{-1}\) are detected from shifted IS absorption and Ly\( \alpha \) emission (e.g., Shapley et al. 2003, Weiner et al. 2009), and from broad FWHM \( \sim 400–500 \) km s\(^{-1}\) emission in H\( \alpha \), [N\( II \)], and [S\( II \)] on galactic and sub-galactic scales (e.g., Genzel et al. 2011, Newman et al. 2012a,b). In deep \( \sim 1–2 \) kpc resolution IFU+AO observations, the broad emission arises from extended regions across the galaxies and is often enhanced near bright star-forming clumps. The line excitation properties are consistent with dominant photoionization by young stars and possibly modest contribution by shocks. Faster AGN-driven winds with velocities up to a few 1000 km s\(^{-1}\) in \( z \sim 2 \) galaxies hosting luminous log(\( L_{\text{AGN}} \)/erg s\(^{-1}\)) > 45 AGN are identified from various rest-UV/optical tracers (see reviews by Fabian 2012, Heckman & Best 2014). In near-IR observations, spatially extended broad emission with typical FWHM \( \sim 1000–2000 \) km s\(^{-1}\) is detected in Balmer as well as forbidden [N\( II \)], [S\( II \)], and [O\( III \)] emission (precluding significant contribution from high-density broad-line region gas; Nesvadba et al. 2008, Cano-Díaz et al. 2012, Genzel et al. 2014b, Cresci et al. 2015). It typically originates from the center of galaxies, can extend over 5–10 kpc for luminous QSOs, and both broad and narrow component line ratios indicate high excitation.

SF- and AGN-driven winds follow distinct demographic trends, most clearly revealed in a recent near-IR IFU study of a sample of \( \sim 600 \) primarily mass-selected galaxies at 0.6 < \( z \) < 2.7, covering a wide range in both mass and star formation activity levels (9.0 < log(\( M_\star / M_\odot \)) < 11.7 and −3.6 < \( \Delta \text{MS} \) < 1.2, see Figure 5; Forster Schreiber et al. 2019). SF-driven outflows are observed at all masses, with an incidence that correlates mainly with star formation properties, and more specifically the MS offset, specific and absolute SFR, and \( \Sigma_{\text{SFR}} \). In contrast, the incidence of AGN-driven outflows (identified based on the combination of rest-optical line profiles and multi-wavelength AGN diagnostics) depends strongly on stellar mass and measures of central stellar mass concentration, irrespective of the level and intensity of star formation activity. The strong differentiation in resulting stacked spectra and decoupling in incidence trends suggest little cross-contamination between dominant SF- and AGN-driven winds.

Several aspects are important in interpreting demographics and comparing between studies. In both nebular emission and IS absorption tracers, the ability to detect an outflow depends on the strength of the wind signature (along with S/N and spectral resolution of the data), such that the trends in incidence partly reflect trends in outflow properties. Slower or weaker winds are more difficult to detect, especially in nebular lines because of the blending with emission from star formation, which underscores the advantage of IFU data in enabling the removal of large-scale orbital motions of the host galaxy. IS absorption features integrate along the line of sight, are sensitive to outflowing material over a wider range and to lower gas densities, and probe material over physical scales up to tens of kpc hence plausibly average over longer timescales. In turn, the emission line technique is more sensitive to denser material closer to the launching sites (as evidenced by high-resolution
Figure 8

Distinction between star formation- and AGN-driven ionized gas winds at $z \sim 1 - 3$ (top and bottom rows, respectively), in terms of spatial, spectral, and demographic properties (left to right). The maps show two galaxies observed with SINFONI+AO and HST at FWHM resolution of $\sim 1.8$ kpc, with the stellar rest-optical light and narrow H$\alpha$ emission from star-forming regions shown in red and green colors, and the broad H$\alpha$+[NII] outflow emission shown in white contours. The composite spectra are constructed from near-IR IFU observations with KMOS and SINFONI, where the continuum was subtracted and large-scale orbital motions were removed based on the narrow H$\alpha$ velocity maps prior to stacking. The demographic trends are based on the fraction of individual objects exhibiting the spectral signatures of SF- and AGN-driven outflows. Figure based on data published by Newman et al. (2012a) and Förster Schreiber et al. (2014, 2019).

IFU maps), making it a more instantaneous probe of outflows. Differences in spatial scales probed, along with possibly less collimated winds in “puffier” higher $z$ galaxies (Law et al. 2012c), may lead to different dependences with galaxy inclination. Given the trends with galaxy properties discussed below, results will also depend on the sample selection and parameter space coverage.

For SF-driven winds, qualitatively similar trends in incidence, or in strength and velocity width of the wind signature, with measures of star formation activity have been found in many other studies. Quantitatively, there are some notable differences especially between studies using different techniques. For instance, among the full near-IR sample studied by Förster Schreiber et al. (2019), the global fraction of SF-driven outflows is $\sim 11\%$, reaches $\sim 25\% - 30\%$ at $\Delta MS \gtrsim 0.5$ dex or $\Sigma_{SFR} \gtrsim 5 - 10$ M$_\odot$ yr$^{-1}$ kpc$^{-2}$; no strong trend with galaxy inclination is found (see also, e.g., Newman et al. 2012b). These fractions are lower than the $\gtrsim 50\%$ based on the occurrence of blueshifted IS absorption lines after accounting for anisotropic geometry (trends with inclination in these studies are stronger) and clumpiness of the outflowing gas (e.g., Weiner et al. 2009, Kornei et al. 2012). These
differences in incidence are consistent with different physical and time scales of outflows probed by each technique and possibly reflect differences in sample selection (mass- vs. UV-selected). The interdependence between SFR, $M_\star$, and $z$, and the choice of criteria employed to identify/exclude AGN, may introduce residual trends with $M_\star$ (e.g., Weiner et al. 2009; Freeman et al. 2019; Swinbank et al. 2019). In general, SF-driven outflows appear to become most prominent above $\Sigma_{\text{SFR}} > 0.5 - 1 \, M_\odot \, \text{yr}^{-1}$, suggesting a higher threshold for wind breakout that may be related to the geometrically thicker, denser, and more turbulent ISM in high $z$ galaxies (e.g., Newman et al. 2012b; Davies et al. 2019).

Turning to AGN-driven outflows, near-IR studies considering the full galaxy population highlighted a steep increase in incidence towards higher masses, most pronounced above $\log(M_\star/M_\odot) \sim 10.7$ (e.g., Genzel et al. 2014b; Förster Schreiber et al. 2019; Leung et al. 2019), qualitatively tracking the behavior for AGN fractions identified in flux-limited surveys (e.g., in X-rays; see Section 3.7). The tight positive trends with measures of central stellar mass concentration (such as $\Sigma_\star$ and $\Sigma_{1\text{kpc}}$; Förster Schreiber et al. 2019; see also Wisnioski et al. 2018) may not be surprising in light of the observed correlations between these properties and $M_\star$, and the elevated fraction of AGN among compact SFGs in $\log(M_\star/M_\odot) > 10$ samples (e.g., Barro et al. 2014a; Rangel et al. 2014; Kocevski et al. 2017). Among AGN, the frequency and/or velocities of outflows appears to increase with $L_{\text{AGN}}$, consistent with simple expectations where more luminous AGN can drive more powerful winds (e.g., Harrison et al. 2012, 2016; Brusa et al. 2015a; Leung et al. 2019). In terms of absolute fractions, most studies imply fairly large outflow fractions among AGN, in the range $\sim 50\%-75\%$ except for Leung et al. (2019), who report a lower 17% incidence (but similar trends with galaxy and AGN properties). Leung et al. (2019) noted in their sample that the outflow fraction among AGN is roughly constant with $M_\star$, and so is $L_{\text{AGN}}$, concluding that AGN can drive an outflow with equal probability irrespective of the host galaxy mass and that observed trends among the full galaxy population reflect those in AGN luminosity coupled with a (mass-independent) Eddington ratio distribution. Detailed comparisons between all studies are still hampered by the heterogeneity in sample size, selection, AGN and outflow identification, data sets (IFU vs. slit spectra) and S/N, but broadly support the picture that more powerful AGN-driven outflows become common in the most massive galaxies.

### 4.6.2. Properties of star formation-driven winds

Outflow velocity, mass, momentum, and energy properties across the galaxy population are essential to constrain the physical drivers of winds and impact of stellar feedback on the evolution of galaxies (e.g., Dutton & van den Bosch 2009; Davé et al. 2017). By necessity, many simplifications are involved in interpreting the data of high $z$ galaxies, usually in the context of idealized models consisting of a conical or spherical geometry, with the velocity distribution, extent, and gas mass being the main parameters. In the theoretical framework, the outflow velocity is generally assumed to be close to the escape velocity, such that $v_{\text{out}} \propto v_c$. Energy and momentum conservation arguments lead to mass loading factors $\eta \propto v_c^{-2}$ for energy-driven winds and $\eta \propto v_c^{-1}$ for momentum-driven winds, where $\eta = M_{\text{out}}/\text{SFR}$ and $M_{\text{out}}$ is the mass outflow rate (e.g., Murray et al. 2005; Oppenheimer & Davé 2006). With $v_c \propto M_{\text{bar}}^{1/3}$ or $\propto M_\star^{1/3}$ (e.g., Mo et al. 1998) and $M_\star \propto \text{SFR}$ on the MS, $\eta$ is expected to follow a power-law with stellar mass and SFR with index $-2/3$ or $-1/3$ for energy- or momentum-driven winds, respectively. There is a strong predicted differentiation in $v_{\text{out}} \propto \Sigma_{\text{SFR}}^\alpha$ with $\alpha \sim 0.1$ for energy-driven winds and $\alpha \sim 2$ for momentum-driven winds (e.g., Strickland et al. 2004; Murray et al. 2005, 2011). These scalings are consistent with recent cosmological zoom
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\( v_{\text{out}} \): Outflow velocity, estimated from the profile of the emission or absorption line wind tracer. Methods based on the centroid or median velocity shift relative to the systemic value probe the bulk of outflowing gas. Other methods including the line width at a fraction of peak amplitude or of cumulative flux/absorption probe the wind velocity distribution.

\( R_{\text{out}} \): Outflow radial extent, most easily and directly obtained from maps of emission tracing the wind gas.

\( n_{\text{e,out}}, N_{\text{H}} \): Local electron density and hydrogen column density of the outflowing gas.

\( M_{\text{out}} \): Mass of outflowing material; it is \( \propto L_{\text{br}}^{-1} n_{\text{e,out}} \) for ionized gas emission tracers where \( L_{\text{br}} \) is the luminosity of the broad outflow-related line component, and \( \propto N_{\text{H}} R_{\text{out}} v_{\text{out}} \) for IS absorption tracers.

\( \dot{M}_{\text{out}} \): Mass outflow rate, estimated as \( M_{\text{out}} \times (v_{\text{out}}/R_{\text{out}}) \).

\( \eta \): Mass loading factor, the ratio \( \dot{M}_{\text{out}}/\text{SFR} \).

\( \dot{E}_{\text{out}}, \dot{p}_{\text{out}} \): Outflow energy and momentum rates, \( \frac{1}{2} M_{\text{out}} v_{\text{out}}^2 \) and \( M_{\text{out}} v_{\text{out}} \); the ratio with stellar or AGN luminosity \( L \) and momentum rate \( L/c \) constrains the wind power source and driving mechanism.

\( L_{\text{SFR}}, L_{\text{AGN}} \): Bolometric luminosity of the stellar population, dominated by young massive stars such that \( L_{\text{SFR}} \sim 10^{10} \text{SFR} \), and from the AGN, estimated from, e.g., X-ray, SED modeling, or nebular line emission.

Measurements of \( v_{\text{out}} \) rely on parametrizations of the observed line profiles, and various approaches have been followed depending on the diagnostic and the data set (e.g., based on the FWHM or full width at zero power of emission tracers, centroid or fractional absolute or cumulative absorption for IS lines). Despite these differences, studies generally find results consistent with \( v_{\text{out}}/v_c \) ratios within a factor of a few around unity, with a linear or slightly sub-linear \( v_{\text{out}} \sim v_c \) trend (e.g., Weiner et al. 2009, Erb et al. 2012, Davies et al. 2019, Förster Schreiber et al. 2019, Swinbank et al. 2019). Given that the escape velocity \( v_{\text{esc}} \approx 3 v_c \) for realistic halo mass distributions (Binney & Tremaine 2008), these results indicate that the higher velocity tail of the outflowing gas may escape from galaxies, and more easily so in lower-mass galaxies, but that recycling may not be negligible.

The broad H\( \alpha \) emission is well suited to estimate mass outflow rates and energetics. Assuming case B recombination and an electron temperature \( T_e = 10^4 \text{ K} \), the mass of ionized gas in the outflow can be estimated via \( M_{\text{out}} \propto L_{\text{br,0}}(\text{H} \alpha)^{1/3} n_{\text{e,out}} \) where \( L_{\text{br,0}}(\text{H} \alpha) \) is the intrinsic luminosity in the broad emission component and \( n_{\text{e,out}} \) is the local electron density, from which the mass outflow rate can be computed as \( \dot{M}_{\text{out}} = M_{\text{out}} (v_{\text{out}}/R_{\text{out}}) \) where \( v_{\text{out}} \) and \( R_{\text{out}} \) are the outflow velocity and extent (e.g., Genzel et al. 2011, Newman et al. 2012a). Calculations typically assume H dominates the mass and apply a 36% mass correction for He. Based on these relationships, \( \eta \) estimates in the range \( \sim 0.1 \) up to above unity were derived on galactic and sub-galactic scales (e.g., Genzel et al. 2011, Newman et al. 2012a,b, Förster Schreiber et al. 2019, Davies et al. 2019, Freeman et al. 2019, Swinbank et al. 2019).

While details in assumptions and samples vary among studies, a key difference lies in the adopted value for \( n_{\text{e,out}} \), which ranges between \( \sim 50 \) and \( \sim 400 \text{ cm}^{-3} \). No significant or mildly positive trends of \( \eta \) with stellar mass were found in the larger samples spanning \( 9.0 \lesssim \log(M_*/M_\odot) \lesssim 11 \), assuming a constant \( n_{\text{e,out}} \) (e.g., Förster Schreiber et al. 2019, Freeman et al. 2019, Swinbank et al. 2019). Estimates based on IS absorption features depend more importantly on geometrical factors, as the absorption strength traces the gas columns along simulations of high \( z \) galaxies (e.g., Hopkins et al. 2012, Muratov et al. 2015).
the line of sight, with \( M_{\text{out}} \propto C_O C_f N_\text{H} v_{\text{out}} \) (where \( C_O \) and \( C_f \) are the angular and clumpiness covering fractions, and \( N_\text{H} \) is the column density), as well as ISM chemistry and radiative transfer effects on the line profiles (e.g., Veilleux et al. 2005). Under reasonable assumptions, \( \eta \sim 1 \) were found in outflow studies of SFG samples employing this technique (e.g., Weiner et al. 2009, Kornei et al. 2012). Comparing wind momentum and energy rate, \( p_{\text{out}} = M_{\text{out}} v_{\text{out}} \) and \( E_{\text{out}} = 0.5 M_{\text{out}} v_{\text{out}}^2 \), to the momentum and luminosity input from star formation \( \dot{p}_{\text{rad}} = L_{\text{SFR}}/c \) and \( L_{\text{SFR}} \), most results are in the ranges \( \dot{p}_{\text{out}}/\dot{p}_{\text{rad}} \sim 0.1 - 1 \) and \( E_{\text{out}}/L_{\text{SFR}} \sim 10^{-4} - 10^{-3} \) and thus consistent with momentum-driven winds powered by the star formation activity (e.g., Genzel et al. 2011, Newman et al. 2012a, Förster Schreiber et al. 2019), but see Swinbank et al. 2019 for a contrasting result. Trends of \( v_{\text{out}} \propto \Sigma_{\text{SFR}}^{0.2-0.4} \) found in other studies from emission and IS absorption diagnostics suggest a possible mixture of momentum- and energy-driving (e.g., Weiner et al. 2009, Davies et al. 2019).

Estimates of \( n_{e,\text{out}} \) through the density-sensitive but weak \( [S \text{ II}] \lambda\lambda6716,6731 \) doublet have long been hampered by S/N limitations. A first reliable broad+narrow Gaussian decomposition in very high S/N stacked spectra (Figure 8, Förster Schreiber et al. 2019) yielded \( n_{e,\text{out}} \sim 380 \text{ cm}^{-3} \) for the outflowing gas (and \( n_{e,\text{III}} \sim 75 \text{ cm}^{-3} \) for the narrow star formation-dominated component). These results suggest the outflowing gas may experience compression, supported by enhanced broad component \( [N \text{ II}]/\text{H} \alpha \) ratios in the same stacks as well as from multiple diagnostic (total) line ratios for some bright individual star-forming clumps (Newman et al. 2012a) and samples with multi-band near-IR spectra (Freeman et al. 2019). Different outflow gas densities adopted in the literature can account for much of the differences in \( \eta \) and other outflow properties, as the observables themselves (broad-to-narrow \( \text{H} \alpha \) flux ratio, \( v_{\text{out}} \), and \( R_{\text{out}} \)) are fairly comparable. With the new evidence suggesting higher \( n_{e,\text{out}} \), a lower range of \( \eta \) (<1) in the warm ionized gas phase would seem favored.

Taken at face value, low mass loading factors and the lack of evidence for an anti-correlation with galaxy stellar mass appear to be in tension with theoretical expectations and numerical simulations, for which \( \eta \gtrsim 0.3 - 1 \) at \( \log(M_*/M_\odot) \sim 10 \) and \( \eta \propto M_*/C_\alpha \) with \( \alpha \) in the range \(-0.35 \to -0.8 \) (e.g., Lilly et al. 2013, Muratov et al. 2015). The tension is compounded by the \( v_{\text{out}} \) results suggesting that some fraction of the outflowing gas may not be able to escape from the galaxy’s potential (reducing the effective \( \eta \)). Notwithstanding all the simplifications made and large uncertainties, the mass outflow, momentum, and energy rates discussed above almost certainly represent lower limits as they miss potentially important wind phases, as seen in local starburst galaxies where the neutral and cold molecular phases dominate the mass and the hot phase dominates the energetics (e.g., Veilleux et al. 2005, Heckman & Thompson 2017).

### 4.6.3. Properties of AGN-driven winds

The role of ejective AGN feedback through “QSO mode” has been much debated in the recent observational literature. At high \( z \), while individual luminous AGN may drive sufficiently massive and energetic outflows to suppress star formation in their host (e.g., Cano-Díaz et al. 2012, Cresci et al. 2013, Carniani et al. 2016, Kakkad et al. 2016), QSOs are rare, such that their impact on the massive galaxy population as a whole and in the long run has remained unclear. The more recent studies based on rest-optical emission lines of larger \( z \approx 2 \) samples, encompassing unbiased (mass-selected) populations and/or AGN selected in deep X-ray surveys, both covering broader ranges in AGN luminosities (in some cases down to \( L_{\text{AGN}}/\text{erg s}^{-1} \) \sim 42.5 - 43) are shedding new light on this issue (e.g., Förster Schreiber et al. 2014, 2019, Genzel et al. 2014b, Harrison et al. 2016, Talia et al. 2017, Leung et al. 2019).
A first general conclusion is that with typical high velocities $\sim 1000 \text{ km s}^{-1}$, AGN-driven winds are in principle able to escape the galaxies and even the halo. The outflow velocity appears to depend on $L_{\text{AGN}}$ but otherwise not on galaxy properties such as $M_*$ or SFR, consistent with the AGN as main power source. Double-Gaussian fits to high S/N stacked spectra suggest dense gas with $n_{e,\text{out}} \sim 1000 \text{ cm}^{-3}$ from the [SII] doublet (Figure 8; Förster Schreiber et al. 2019) albeit with significant uncertainties because of the important blending for the broad emission of the fast AGN-driven winds and the doublet ratio reaching towards the high-density limit. Elevated [NII]/H$\alpha$ ratios of $\sim 1 - 2$ in broad and narrow emission alike for a significant subset of this sample suggests an important contribution from shock excitation. Keeping in mind all the uncertainties involved, different assumptions adopted by different authors, and large scatter among galaxies, there is overall agreement that on average the momentum and energy rates of AGN-driven outflows exceed those that could be produced by star formation alone, and are consistent with energy-driving contributing or even dominating (Förster Schreiber et al. 2019; Leung et al. 2019), as also suggested by the $v_{\text{out}}$ dependence on $L_{\text{AGN}}$ (Talia et al. 2017; Leung et al. 2019). Mass outflow rates (compared to the SFRs) are found to be modest to low ($\eta \lesssim 1$) on average among SFGs, and possibly higher towards the sub-MS regime.

While AGN-driven winds may expel ionized gas at modest rates compared to the SFRs (similarly to the SF-driven outflows), they carry substantial amounts of momentum and energy ($\sim 10$ times or more than the SF-driven winds). If more mass, momentum, and energy are contained in other wind phases (or if $n_{e,\text{out}}$ estimates are lower than adopted), all estimates would increase. Measurements in other phases are still scarce at $z \sim 2$; CO observations suggest $\eta \sim 1$ in two MS SFGs hosting AGN, one of which is a QSO (Herrera-Camus et al. 2019; Brusa et al. 2018). Even if not substantially depleting the gas reservoirs of their host, the high-velocity and energetic AGN-driven winds escaping from the galaxies may interact with halo gas, reach high temperatures with long cooling time, and help prevent further gas infall together with virial shocks. The rapid increase in the incidence of AGN-driven winds among the galaxy population at around the Schechter mass echoing the decline in specific SFR and molecular gas mass fractions (Whitaker et al. 2014; Tacconi et al. 2018) is suggestive of a connection between AGN-driven winds and quenching, although it may not be sufficient alone to establish a causal link. Given the wide range in AGN luminosities and inferred Eddington ratios for the larger samples discussed above, the results appear to be qualitatively in line with suggestions based on recent cosmological simulations that kinetic feedback from SMBHs accreting at low Eddington ratio may be more efficient at quenching star formation through preventive feedback in the circumgalactic medium (Bower et al. 2017; Nelson et al. 2018; Fillepich et al. 2018a).

5. OTHER $z \sim 2$ STAR-FORMING POPULATIONS

We here briefly discuss specific subpopulations among SFGs that have been the focus of dedicated analyses for reasons of their extreme starburst nature and/or their role as candidate immediate progenitors to the accumulating population of quiescent galaxies at cosmic noon. Salient physical features of the latter class of galaxies are summarized as well.
5.1. “MS outliers,” and Submm Galaxies

Whereas normal MS galaxies are predominantly disks, at all epochs a population of starbursting outliers exists that may well result from merging activity. At $z \sim 2$ such starburst galaxies, defined by their SFR being more than four times higher than on the MS, represent only 2% of the mass-selected SFGs, accounting for only 10% of the cosmic SFR density at this epoch (Rodighiero et al. 2011). Modeling the SFR distribution of SFGs at fixed mass with a double gaussian reveals a similar, constant or only weakly redshift-dependent, starburst contribution of 8% – 14% to the overall SFR budget (Sargent et al. 2012).

Structurally, there are indications that above-MS outliers exhibit smaller effective radii and cusplier light profiles than their exponential disk counterparts along the MS ridgeline. This is seen for nearby populations, but in rest-UV/optical and radio observations at cosmic noon as well, albeit with significant scatter and only when collecting samples over wide areas to sample the poorly populated high-SFR tail of the galaxy population (Wuyts et al. 2011b, Elbaz et al. 2011). Splitting the SFG population in below-, on- and above-MS subsets (Nelson et al. 2016b) find the above-MS SFGs to feature enhanced $\text{H}\alpha \Sigma_{\text{SFR}}$ at all radii. Only for $\log(M_*/M_\odot) > 10.5$ is the enhancement particularly seen in the center. It should be noted though that extreme outliers (8× above the MS) have 90% of their star formation revealed only in the far-IR and often are optically thick even in H$\alpha$ (Puglisi et al. 2017).

Beyond structural properties, a systematic increase in gas fraction (e.g., Tacconi et al. 2020), dust temperature (Magnelli et al. 2014), and ratio of total IR to rest-8$\mu$m luminosities (Elbaz et al. 2011, Nordon et al. 2012) is seen as one moves across the MS towards higher SFRs. Not only does the amount of obscuration by dust increase (Wuyts et al. 2011b), the resulting effective attenuation law as imprinted in the IRX-β relation also varies systematically with position in SFR-mass space (Nordon et al. 2013). All of these trends between MS offset and physical diagnostics suggest that the observed scatter around the MS is real, and cannot be fully attributed to measurement uncertainties associated with the various SFR tracers employed. Confirming this point more directly, Fang et al. (2018) demonstrate that independent ∆MS measurements based on 24$\mu$m and UV-to-optical diagnostics correlate significantly.

Predating the terminology of a main sequence and orthogonal to the historical background of rest-UV/optical lookback surveys is the rare population of very luminous high-z Submm Galaxies (SMGs), first discovered in the late 1990s through 850$\mu$m observations with SCUBA on the JCMT (≥ 15″ beam; Smail et al. 1997). Since then, higher resolution far-IR observations have refined our understanding of the nature of SMGs, identifying multi-component morphologies in some and very compact cores with large velocity ranges in other cases (Tacconi et al. 2006, 2008). These results point to merger-driven short-lived (~ 100 Myr) “maximum starburst” events. ALMA 1 mm observations demonstrated that multiplicity of single-dish sources becomes increasingly common towards the bright end, with 28% of $> 5$ mJy sources and 44% of $> 9$ mJy sources being identified as blends (Stach et al. 2018). Using spectroscopic follow-up of individual components for modest samples (Hayward et al. 2018) or a statistical approach based on photometric redshifts for samples of several dozen SMGs (Stach et al. 2018) it is further apparent that both chance alignments and physically associated components make up a significant fraction of the

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SMG: Submm galaxy.

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The non-universality of attenuation law shapes at cosmic noon has also been reported by Salmon et al. (2016) and Reddy et al. (2018), with increasingly shallower slopes towards the more enriched and dustier regime, rooted in changing star – dust geometries and possibly grain size distributions.
blends, with physically associated pairs adding up to at least 30%.

Accounting for multiplicity hence reduces the inferred SFRs for some of the brightest SMGs, relieving some tension with models and bringing them closer to the MS. Their MS offset is further reduced when allowing for multi-component SFHs, which have a tendency of increasing the inferred stellar mass. For this reason, Michałowski et al. (2014) argue that SMGs reside predominantly at the high-mass tip of the MS rather than being positioned above, consequently also questioning their merger nature.

The rarity of above-MS outliers and SMGs can be interpreted in terms of short duty cycles preceding a quenching event. For example, Wuyts et al. (2011b) contrast the number density of ΔMS > 0.5 outliers to the growing number density of quiescent galaxies at cosmic noon inferring timescales of order ~ 100 Myr for the starbursting phase. Toft et al. (2014) take a different approach, in which they contrast the inferred formation redshifts of compact quiescent galaxies at z ~ 2 to the redshift distribution of the 3 < z < 6 SMG population, finding a good match that is further underlined by their similar positions in size-mass space and consistently high characteristic velocities. Assuming an evolutionary connection, they can reconcile their relative space densities by invoking an SMG lifetime of ~ 42 Myr. The relatively short timescales found in the above studies are consistent with the duration of the final merger phase and peak starburst around coalescence of dissipative major mergers (e.g., Mihos & Hernquist 1994 [Hopkins et al. 2006]).

5.2. Compact Star-Forming Galaxies

In order to reveal evolutionary connections between galaxies before and after quenching, a selection on the basis of similar structural properties (i.e., identifying SFGs in the compact corner of size-mass space where high-z quiescent galaxies reside) has become a popular approach (e.g., Barro et al. 2013, 2014a). After z ~ 1.8 the number density of these compact star-forming galaxies (cSFGs) are dropping precipitously, while the number density of compact quiescent galaxies is still rising. Duty cycle arguments akin to those described in the previous Section yield typical lifetimes for this cSFG phase of ~ 500 – 800 Myr, dependent on the precise compactness and star formation selection criteria imposed (Barro et al. 2013, van Dokkum et al. 2015). cSFGs thus represent a longer-lasting phase than the one discussed in Section 5.1 which is also reflected in their larger abundance and larger range in star formation activities, from above to on and below the MS.

A salient feature of the cSFG population is that both X-ray and line ratio diagnostics reveal a very high AGN fraction (≥ 40% based on X-rays and up to ~ 75% when folding in line ratio diagnostics). This enhancement in AGN activity is highly significant relative to quiescent galaxies but also compared to similar-mass SFGs that are more extended (Barro et al. 2014a, Kocevski et al. 2017, Wisnioski et al. 2018). They are further found to be highly obscured, with dust cores even smaller than their stellar extent (Barro et al. 2016, van Dokkum et al. 2015). Resolved gas kinematics of cSFGs have revealed that the large galaxy-integrated linewidths can to a large degree be attributed to unresolved disk rotation (Barro et al. 2017b, Wisnioski et al. 2018). While their stellar distributions are by definition compact, the ionized gas disks are often more extended (van Dokkum et al. 2015, Wisnioski et al. 2015).
et al. 2018). Even when modeled with rotating disks and accounting for inclination and beam-smearing effects the resulting stellar-to-dynamical mass ratios of the more compact SFGs are close to unity and larger than that of extended SFGs (van Dokkum et al. 2015, Wuyts et al. 2016b, Wisnioski et al. 2018). These dynamical measurements support a picture that cSFGs are in their last stretch of star formation with already dwindling gas fractions and short depletion times. Spilker et al. 2016 and Popping et al. 2017 have come to a similar conclusion on the basis of molecular line measurements for this sub-population.

Several lines of evidence highlight the resemblance in dynamical terms between cSFGs and the quiescent population to which they are candidate immediate progenitors. Compact quiescent galaxies at cosmic noon exhibit more flattened projected shapes than anticipated for a pressure supported population (van der Wel et al. 2011, Chang et al. 2013), their $M_{\text{dyn}}/M_*$ ratios calculated from galaxy-integrated stellar velocity dispersions using a virial mass estimator are higher for systems with flatter projected axis ratios (Belli et al. 2017a), and in four gravitationally lensed cases stellar velocity curves reveal unambiguously their rotationally supported nature (Newman et al. 2015, 2018b, Toft et al. 2017), consistent with a highly dissipational formation process (Wuyts et al. 2010, Wellons et al. 2015).

6. THEORETICAL PICTURE AND ADVANCES IN NUMERICAL SIMULATIONS

Models of galaxy formation in a ΛCDM context have seen significant improvements over the past decade. In particular, great strides forward were made in resolving the so-called angular momentum catastrophe (the inability to reproduce the Tully-Fisher and rotation speed - angular momentum relation of observed disks galaxies; Navarro & Steinmetz 2000), and the overproduction of stars in both low- and high-mass galaxies. Cosmological galaxy formation models still feature variations at the factor of ~ 2 level in for example the peak stellar-to-halo mass ratio reached around $M_{\text{halo}} \sim 10^{12} M_\odot$ and possibly more at lower/higher masses, but they now fall within the range of uncertainties from abundance matching estimates that traditionally serve as a benchmark. Today, we face a landscape of theoretical models that can be differentiated by the physical scales they resolve, the numerical techniques they employ, and the (astro)physics they implement. The scales that are resolved dictate which physical properties can be considered “imposed” versus “emerging” from such models (see reviews by Somerville & Davé 2015, Naab & Ostriker 2017).

On the largest scales, semi-analytic models can efficiently imprint the baryonic growth of galaxies on merger trees extracted from DM-only simulations with box sizes of $1-10$ Gpc (Millennium, Millennium-XXL, Bolshoi, Las Damas). Effectively resolving individual galaxies at the halo scale, basic structural properties such as galaxy sizes are then evaluated through analytical recipes that either assume specific angular momentum conservation (Mo et al. 1998) or encode dependencies on both angular momentum and halo concentration (Somerville et al. 2018, Jiang et al. 2019), and are designed to capture processes such as disk instabilities and mergers. For the latter, simple energy conservation arguments are often augmented with calibrations based on idealized merger simulations to account for the impact of dissipative processes on the resulting bulges (Covington et al. 2011). While intrinsically unable to track detailed structural evolution from first principles, such models have the merit of being computationally cheap (7 CPU hours to execute a single realization producing over $10^7$ galaxies). They are therefore the only type of models for which a full exploration of parameter space and a mapping of its degeneracies by means of Monte Carlo
Markov Chains is feasible (e.g., Henriques et al. 2015). Inclusion of hydrodynamics comes at a major computational expense but allows key processes for structural evolution to be resolved rather than prescribed. State-of-the-art full cosmological simulations (Illustris, EAGLE, Magneticum, Horizon-AGN, Illustris TNG, SIMBA) are capable of evolving populations of $10^4 - 10^5$ galaxies in $10 - 300$ Mpc boxes with sufficient resolution (baryonic particle masses of $\sim 10^6 - 10^7$ M$_\odot$, sub-kpc gravitational softening lengths) to track their internal structural development and kinematics. With a temperature floor of $10^4$ K and the reliance on subgrid recipes to infer cold gas fractions, they are complemented by zoom-in simulations of more than 100 times enhanced mass and spatial resolution, which are capable of resolving Jeans mass/length scales, giant molecular cloud formation and a self-consistent modeling of the multi-phase ISM (e.g., FIRE, Auriga, VELA). Further down the series of Russian dolls come simulations of isolated galaxies or ISM slices in an external potential resolved down to parsec scales (e.g., SILCC). They are ideally suited to track the multi-phase breakdown of the ISM including the chemistry of molecular gas formation, the local injection of energy and momentum by late stages of stellar evolution and its coupling to the surrounding medium (e.g., effects of peak driving vs. supernovae exploding after stars migrate away from their birthclouds, ISM porosity and the possibility of feedback energy escaping through the path of least resistance, impact of the IR opacity on the effectiveness of radiation pressure, ...).

The hydro-solvers employed in generating the above multi-scale simulations range from grid-based Adaptive Mesh Refinement (AMR) to Smoothed Particle Hydrodynamics (SPH; with refinements to better capture contact discontinuities and shock fronts, Hopkins 2015), and include hybrid moving mesh approaches (Springel 2010). In common between these models, the physics of gravity, hydrodynamics, cooling and heating, star formation and evolution (SNIa, SNII, AGB), chemical enrichment (tracking up to 11 individual elements), black hole growth, and stellar and AGN feedback are now routinely implemented. Increasingly, also the impact of other processes, such as magnetic fields, radiation pressure, cosmic rays and even the formation and destruction of dust are explored, albeit some of them restricted to the highest resolution simulations only.

Qualitatively, overcoming the hurdles posed by the angular momentum problem and the observed inefficiency of galaxy formation took the implementation of strong feedback processes. How exactly this goal is most realistically achieved through numerical and/or subgrid recipes remains a matter of intense debate, on which resolved observations of galaxy structure and kinematics aim to shed light. Implementations of stellar feedback differ in their injection velocities, mass loadings and directionality, and whether or not wind particles are temporarily decoupled from hydrodynamic interactions to prevent numerical overcooling. Likewise, AGN feedback as a term covers a considerable range of implementations, starting from the choice of black hole seeding, whether or not boosting factors are applied to conventional Bondi accretion, directionality and continuity/stochasticity with which gas particles are being heated or receive kinetic kicks. Different choices are made regarding which gas particles this thermal/kinetic energy is imparted on, and whether (e.g., Illustris TNG) or not (e.g., EAGLE) different prescriptions are applied in the high vs. low accretion rate regime. Consequently, predictions on key wind properties are still in flux, with for example TNG winds being faster but of lower mass loading than those in its Illustris precursor. This illustrates the continued need for empirical guidance.

Last but not least, significant work on the interface between simulations and observations is enabling ever more consistent comparisons. This starts with the basic question of
what it is that constitutes a galaxy’s stellar mass, and related, what it is that observers are measuring. Pillepich et al. (2018b) illustrate how aperture-based masses (as opposed to total stellar masses integrated out to the virial radius) can significantly alter our view on the stellar mass function and SMHM relation, particularly for the most massive galaxies featuring extended wings, but even so at the knee of the SMHM relation. Bringing the models yet more into the observational realm, post-processing with advanced radiative transfer techniques (SKIRT, Sunrise, Powderday) are enabling mock observations accounting for the effects of light weighting, dust extinction and reprocessing, including also ionized and molecular gas line emission. These can aid refined calibrations of observational diagnostics and SED modeling techniques, and are adopted in feasibility studies for upcoming observing facilities.

7. SUMMARY AND OUTLOOK

This article highlighted some of the key insights emerging from increasingly complete population censuses and increasingly detailed studies of individual galaxies back to the cosmic noon epoch. Many global and resolved properties tracing the stars, gas, and kinematics are well probed down to log(M/\(M_\odot\)) \approx 10 (or below). Current results draw a consistent broad picture (see Summary Points) and raise the next questions for future work (see Future Issues for a selection). The knowledge gained from these observations has contributed to transform — in some aspects, profoundly — our view of galaxy evolution. The emerging picture is encapsulated in the equilibrium growth model summarized in Section 1.1, and discussed by Tacconi et al. (2020) in relation to the evolution of the characteristic timescales of the processes controlling galaxy growth including cosmic accretion, merging, galactic gas depletion and star formation, internal dynamics, and gas recycling.

The state-of-the-art in our knowledge of the properties of \(z \approx 2\) SFGs is illustrated in Figures 9 and 10. The censuses and scaling relations allow a depiction of the evolutionary and dynamical state of SFGs in relation to the MS. Coupled with the assumption that mass-ranking of galaxies is conserved, this cross-sectional view of the galaxy population at different epochs can be translated to tracks representing the average evolution of individual galaxies. The outcome of such an approach is shown in Figure 9 for a galaxy reaching the stellar mass of the Milky Way by the present day. Cosmic noon is the main formation epoch of stars in \(z \approx 0\) galaxies of masses similar and up to \(\sim 2 \times \) higher than the Milky Way (log(M/\(M_\odot\)) \approx 10.7 – 11), which account for as much as \(\sim 25\%\) of the local stellar mass budget. In turn, resolved mapping is now possible for various tracers of the baryon cycle from gas and star formation to metal enrichment and feedback, of the dynamical state, of processes leading to the build-up of galactic components and their imprint on the distribution of stars. Such comprehensive sets at the currently best achievable \(\sim 1\) kpc resolution (unlensed) are still limited to small numbers of \(z \approx 2\) SFGs; Figure 10 shows one example.

SUMMARY POINTS

1. Two key observational aspects have driven major advances in our understanding of how galaxies evolved since cosmic noon by providing unparalleled comprehensive views of distant galaxies: (i) the concentration in “legacy cosmological fields” of photometric and spectroscopic surveys across the electromagnetic spectrum, and (ii) the growing samples with stellar structure, star formation, and gas kinematics.
resolved on subgalactic scales. Mass selection is routinely used, allowing more complete population-wide censuses of physical processes driving galaxy evolution.

2. Scaling relations between galaxy stellar mass, SFR, metallicity, gas content, size, structure, and kinematics are in place since at least $z \sim 2.5$, indicating that regulatory mechanisms start to act on galaxy growth within 2–3 Gyr of the Big Bang. There is significant evolution in population properties: compared to $z \sim 0$, typical SFGs at $z \sim 2$ were forming stars and growing their central SMBH $\sim 10 \times$ faster from $\sim 10 \times$ larger cold molecular gas reservoirs. Disks are prevalent but smaller, more turbulent, and thicker than today’s spirals. Quenching was underway at high masses, through mechanisms that appear to largely preserve disky structure.

3. Resolved stellar light, star formation, and kinematics on scales down to $\sim 1$ kpc point to spatial patterns — more pronounced in higher mass SFGs — from dense and strongly baryon-dominated core regions with possibly suppressed star formation to more actively star-forming outskirts. Whether these patterns reflect inside-out growth/quenching scenarios, or carry the imprint of strong radial gradients in extinction and efficient dissipative processes in gas-rich disks is open. The detection of large nuclear concentrations of cold gas and kinematic evidence of radial inflows in the most massive galaxies support the latter scenario, in which case massive but highly obscured stellar bulges may still be rapidly growing.
State-of-the-art observations detailing the evolutionary state and probing the baryon cycle of a $z = 2.2$ massive MS galaxy ($M_\star \sim 10^{11} \, M_\odot$). The maps show, clockwise from the top left, the rest-frame UV and $U$ band emission dominated by unobscured continuum light from young massive stars; H$\alpha$ emission from moderately unobscured HII regions; CO(4−3) emission revealing the cold molecular gas fueling largely obscured star formation; rest-frame $\sim 5000$ Å light tracing the bulk of stars; the stellar mass distribution; H$\alpha$ velocity field and dispersion map tracing gravitational motions; broad low-amplitude emission in H$\alpha$+[NII] revealing high-velocity outflowing gas; [NII]/H$\alpha$ ratio sensitive to the excitation and physical conditions of the nebular gas. The FWHM resolution is shown by the white ellipse in each panel. Despite a clumpy appearance in UV/optical stellar light and H$\alpha$, the kinematics and stellar mass map reveal a massive rotating yet turbulent disk hosting a dense bulge-like component. The bulge may still be growing out of the massive central molecular gas reservoir, which may be replenished through inward gas streaming along a bar or spiral arms as hinted at by the inner isovelocity twist, double-peaked central dispersion, and $\sim 5000$ Å morphology. The weak [NII]/H$\alpha$ radial gradient in the outer disk could indicate a shallow metallicity gradient, consistent with efficient metal mixing within the turbulent gas disk and/or through galactic outflows. The elevated [NII]/H$\alpha$ $\sim 0.7$ at the center signals the presence of a (low-luminosity) AGN. Ionized gas is being driven out of the galaxy through star formation feedback near the location of the brightest UV/optical/H$\alpha$ clump, as well as through AGN-driven feedback near the nucleus. Based on data presented by Förster Schreiber et al. (2011, 2018), Tacchella et al. (2018), and obtained from the ALMA archive (program 2013.1.00059.S, PI Aravena).

4. Outflows traced by warm ionized and neutral high-velocity gas act across a wide swath of the galaxy population. SF-driven winds dominate below the Schechter mass and are more ubiquitous and/or stronger at higher star formation levels, but may largely remain bound to the galaxy. AGN-driven winds dominate at higher masses, with rapidly rising incidence and/or strength with stellar mass and central concentration thereof. Improved constraints suggest dense, possibly shocked-compressed ionized material in both outflow types, leading to modest sub-unity
mass loading factors in the warm ionized phase. The high duty-cycle AGN-driven winds are sufficiently fast to escape their massive host and heat halo gas, tantalizingly suggesting a preventive form of AGN feedback contributes to quenching.

**FUTURE ISSUES**

1. What is the origin of scatter in galaxy scaling relations (between $M_\star$, SFR, size, gas content, metallicity, ...)? Is any scatter around the observed relations attributed to short-term stochasticity (i.e., the equivalent of “weather”) or an imprint of a long-term differentiation in growth histories among SFGs of the same mass at a given epoch? If the latter, what (halo) property other than mass is most appropriate to describe the SFG population as a two-parameter family?

2. What is the physics responsible for setting the gas turbulence? The redshift evolution of $\sigma_0$ can be understood in the framework of marginally stable disks with gas fractions that are dwindling with cosmic time. Yet, at fixed redshift, no clear correlation with galaxy properties is emerging that would unambiguously identify the main driver of turbulence. Is this because of limited dynamic range sampled, significant contributions from unresolved non-circular motions, other observational factors? Results from strongly-lensed galaxies indicate elevated dispersions on scales down to a few 100 pc, but samples are still small and limited in galaxy mass coverage. Tighter constraints on spatial variations and anisotropy (as observed in nearby disks) will be helpful in addressing these questions.

3. What is the origin of the high baryon fractions and concentrations of SFGs? A robust trend of increasing baryon fractions with redshift up to $z \sim 2.5$, and a correlation with increasing surface density, are emerging from disk modeling of IFU kinematics. Several lines of empirical evidence, supported by theoretical work, point to the important role of efficient transport of material from the halo to the disk scale and further inwards to the bulge in the gas-rich high $z$ disks. More direct constraints are needed on gas inflows onto and within galaxies, and on the relative importance of radial transport vs. inside-out growth in setting the structure of galactic components and, possibly, contributing to star formation quenching.

4. Where do massive $z \sim 2$ SFGs form their last stars before they get quenched? Balmer decrement maps for individual galaxies and bolometric UV+IR SFR maps accounting for potential gradients in dust temperature will be required to address whether half-SFR sizes at the tip of the MS are smaller than, equal to, or larger than the half-stellar mass sizes inferred from multi-wavelength HST imagery.

5. What are the total mass loading and energetics of galactic-scale winds, and the breakdown into multi-phase components? Much of our knowledge about wind properties and demographics is based on the warm ionized and neutral phase. A more holistic view on wind properties and their impact on galaxies will strongly benefit from the combination of multi-phase tracers, still limited to small numbers of more extreme objects and very few normal MS SFGs at high $z$. A few pilot programs suggest that, akin to what is seen in nearby starbursts, the bulk of the mass flow may be in the molecular phase, highlighting the importance of cold molecular gas
kinematics to fully capture their role in galaxy evolution and baryon cycling.

6. What are the exact mechanisms responsible for the shutdown of star formation in massive galaxies? The increase in the prevalence of massive bulges, dense cores, and powerful AGN and AGN-driven outflows at high galaxy masses, where the specific SFR and cold gas mass fractions drop, suggest they likely play a role in galaxy quenching. The evidence of an association with quenching, however, remains to date largely circumstantial, and further observational constraints are needed to pin down the mechanism(s) at play and establish causality.

7. How do galaxies below $\sim 10^{9-9.5} M_\odot$ fit into the emerging picture anchored in the properties of higher mass populations? Low-mass galaxies are still poorly explored because of current observational limitations. If an increasing proportion of the low-mass population has prolate/triaxial structure, how can we interpret their kinematics until we can fully resolve them? Do scaling relations break down at these masses?

The outlined questions, among others, frame the observational (and theoretical) landscape for the next decade, with exciting progress anticipated from developments on the instrumentation scene. NOEMA and ALMA are leveraging our knowledge about the stellar component and ionized gas with that of the cold molecular gas. The combination of the multi-IFU KMOS and the new sensitive AO-assisted ERIS single-IFU at the VLT will expand samples with kinematics, star formation, and ISM conditions from near-IR observations, and resolve them on sub-galactic scales down to $\sim 1$ kpc. JWST at near- and mid-IR wavelengths will open up an unprecedented window on the earliest stages of galaxy evolution, charting the progenitor populations of cosmic noon galaxies. The giant leap in resolution afforded by diffraction-limited instruments on the next generation of 25-40 m-class telescopes, such as the first-light imager and spectrometer MICADO and the IFU HARMONI at the ELT, will be the next game-changers (Figure 11). With unparalleled sharp views of the galaxy population on the scales of individual giant molecular cloud and star-forming complexes, the era of extremely large telescopes will undoubtedly dramatically boost our knowledge and change our approach to studying galaxy evolution across all times.
Illustration of the gain in angular resolution from current to future facilities. For this simple illustration, optical imaging of the nearby M83 spiral galaxy (at a distance of 4.5 Mpc, based on data presented by Larsen & Richtler [1999]) is redshifted to $z = 2$ and boosted up in luminosity by a factor of $\sim 20$ (following the MS evolution) but no other evolution is considered (e.g., in size or gas fraction). The left panel shows the original color-composite map at a resolution corresponding to 35 pc. Successive panels to the right are simulated color-composite images for observations with HST and AO-assisted instruments on 8 m-class telescopes at a resolution of $\sim 1.5$ kpc, with the JWST/NIRCAM imager at a resolution of $\sim 700$ pc, and with the ELT/MICADO+AO first-light instrument reaching a diffraction-limited resolution of $\sim 100$ pc (pixel sampling is adjusted for each instrument). Simulations with the SimCADO software [Leschinski et al. 2016] indicate that compact cluster-like sources with luminosities comparable to those of bright super star clusters in nearby starburst galaxies can be detected and characterized with on-source integrations of a few hours. Such objects at $z \sim 2$ might be progenitors to today’s metal-rich globular cluster population (e.g. Shapiro et al. 2010).

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SUPPLEMENTAL TABLES

The Tables below are associated with Figures 2 and 3 of the main article, which feature a selection of extragalactic surveys providing relevant samples at cosmic noon epochs, either specifically targeting objects or having a significant number of sources overlapping with the $1 \leq z \leq 3$ interval. Table 1 lists the photometric and spectroscopic surveys, acronyms or brief description, and the main reference for the source catalogs used in Figure 2. Table 2 focusses on the near-IR IFU surveys plotted in Figure 3, with their acronyms or brief description, the main IFU instrument and observing mode used, and the reference for the published galaxy sample properties.
| Table 1 Photometric and Spectroscopic Surveys |
|---------------------------------------------|
| **Survey**                                   |
| **Full Name or Description**                 |
| **Reference(s)**                             |
|---------------------------------------------|
| Wide-field Ground-based Multi-band Photometric Imaging Surveys | KiDS+VIKING-450 | Wright et al. (2019) |
| Hyper Suprime-Cam Subaru Strategic Program (Wide, Deep, UltraDeep) | HSC-SSP | Aihara et al. (2018) |
| BM/BX/LBG Imaging campaigns centered on QSO fields | Steidel et al. (2003, 2004) |
| COSMOS Cosmic Evolution Survey (COSMOS2015 catalog) | COSMOS | Scoville et al. (2007a), Laigle et al. (2016) |
| CANDELS Cosmic Assembly Near-infrared Deep Extragalactic Legacy Survey | CANDELS | Grogin et al. (2011), Koekemoer et al. (2011) |
| Multi-wavelength Survey by Yale-Chile / Extended Chandra Deep Field South | MUSYC/ECDFS | Cardamone et al. (2010) |
| FourStar Galaxy Evolution survey | zFOURGE | Straatman et al. (2016) |
| All-wavelength Extended Groth strip International Survey, NEWFIRM Medium Band Survey | AEGIS | Davis et al. (2007), Whitaker et al. (2011) |
| Hubble Frontier Fields Treasury Survey (HFF-DeepSpace catalog) | HFF | Lotz et al. (2017), Shipley et al. (2018) |
| HST WFC3/G141 grism spectroscopic surveys | 3D-HST/AGHAST | Momcheva et al. (2016) |
| WFC3 Infrared Spectroscopic Parallel surveys | WISPs | Atek et al. (2010), Colbert et al. (2013) |
| Grism Lens-Amplified Survey from Space | GLASS | Treu et al. (2015) |
| Keck/DEIMOS spectroscopic surveys | DEEP2/DEEP3 | Newman et al. (2013), Cooper et al. (2012) |
| VIMOS VLT Deep Survey | VUDS | Le Fèvre et al. (2015), Tasca et al. (2017) |
| VIMOS survey of the CANDELS CDFS and UDS fields | VANDELS | McLure et al. (2018), Pentericci et al. (2018) |
| Compilation of optical spectroscopic redshifts from multiple programs in GOODS-North | GOODS-N | Barger et al. (2008) |
| Compilation of optical spectroscopic redshifts from multiple programs in GOODS-South | GOODS-S | Master Catalog v3.0 (excluding VVDS) |
| Keck Baryonic Structure Survey with LRIS (optical), MOSFIRE (near-IR) | KBSS-UV/-MOSFIRE | Steidel et al. (2014), Strom et al. (2017) |
| Subaru/FMOS near-IR galaxy redshift survey | FastSound | Tonegawa et al. (2015), Okada et al. (2016) |
| Subaru/FMOS near-IR spectroscopic survey in COSMOS | FMOS-COSMOS | Kashino et al. (2019) |
| MOSFIRE Deep Evolution Field survey (near-IR) | MOSDEF | Kriek et al. (2015) |
| Keck/MOSFIRE near-IR spectroscopic survey in rich environments | zFIRE | Nanayakkara et al. (2016) |
| Team Keyhole Survey in near-IR with MOSFIRE | TRESS | |
| Survey                 | Full Name or Description                          | Instrument and mode<sup>a</sup> | Redshifts | Reference(s)                                      |
|-----------------------|--------------------------------------------------|---------------------------------|-----------|---------------------------------------------------|
| KMOS<sup>3D</sup>     | KMOS IFU survey across cosmic noon                | KMOS, no-AO                    | 0.6 – 2.7 | Wisnioski et al. (2015, 2019)                     |
| KROSS                 | KMOS Redshift One Spectroscopic Survey           | KMOS, no-AO                    | 0.6 – 1.0 | Stott et al. (2016), Harrison et al. (2017)       |
| KGES                  | KMOS Galaxy Evolution Survey                     | KMOS, no-AO                    | 1.3 – 1.5 | Gillman et al. (2020)                             |
| KDS                   | KMOS Deep Survey                                 | KMOS, no-AO                    | 3.1 – 3.8 | Turner et al. (2017)                              |
| KLEVER<sup>b</sup>    | KMOS LENsed galaxies Velocity and Emission line | KMOS, no-AO                    | 1.2 – 2.5 | Curti et al. (2020)                               |
| KLASS<sup>c</sup>     | KMOS Lens-Amplified Spectroscopic Survey         | KMOS, no-AO                    | 0.6 – 2.3 | Mason et al. (2017), Girard et al. (2020)         |
| KLENS                 | KMOS LENsing Survey                              | KMOS, no-AO                    | 1.2 – 3.6 | Girard et al. (2018)                              |
| KASHz<sup>b</sup>     | KMOS AGN Survey at High redshift                | KMOS, no-AO                    | 0.6 – 2.6 | Harrison et al. (2016), Scholtz et al. (2020)      |
| SINS/zC-SINF          | Spectroscopic Imaging survey in the Near-IR with | SINFONI, no-AO and AO          | 1.3 – 2.6 | Förster Schreiber et al. (2009)                    |
|                       | zCOSMOS-SINF project                             | SINFONI, no-AO                 | 1.3 – 2.6 | Mancini et al. (2011)                             |
| SINS/zC-SINF AO       | AO follow-up of SINS/zC-SINF sample              | SINFONI, AO                    | 1.4 – 2.5 | Förster Schreiber et al. (2018)                    |
| MASSIV                | Mass Assembly Survey with SINFONI in VVDS        | SINFONI, no-AO and AO          | 0.9 – 2.2 | Contini et al. (2012), Epinat et al. (2012)       |
| AMAZE                 | Assessing the Mass-Abundance redshift-[Z] Evolution | SINFONI, no-AO               | 3.0 – 5.1 | Troncoso et al. (2014)                            |
| LSD                   | Lyman-break galaxies Stellar populations and Dynamics | SINFONI, AO               | 2.4 – 3.4 | Troncoso et al. (2014)                            |
| Law09                 | IFU observations of rest-UV-selected galaxies    | OSIRIS, AO                     | 2.0 – 3.3 | Law et al. (2009, 2012)                           |
| W09                   | IFU observations of rest-UV-selected galaxies    | OSIRIS, AO                     | 1.5 – 1.7 | Wright et al. (2009)                              |
| IROCKs                | Intermediate Redshift OSIRIS Chemo-Kinematic Survey | OSIRIS, AO               | 0.8 – 1.4 | Mieda et al. (2016)                               |
| WiggleZ               | IFU follow-up of rest-UV selected galaxies       | OSIRIS, AO                     | 1.3 – 1.5 | Wisnioski et al. (2011)                           |
| SHiZELS               | SINFONI - High-Z Emission Line Survey            | SINFONI, OSIRIS, NIFS, AO      | 0.8 – 3.3 | Gillman et al. (2019)                             |
| Lensed                | Collection of strongly-lensed targets            | SINFONI, OSIRIS, NIFS, AO      | 1.0 – 3.7 | Jones et al. (2010, 2013)                         |
|                       |                                                  |                                 |           | Yuan et al. (2011, 2012)                          |
|                       |                                                  |                                 |           | Wuyts et al. (2014)                               |
|                       |                                                  |                                 |           | Livermore et al. (2015)                           |
|                       |                                                  |                                 |           | Leethochawalit et al. (2016)                      |

<sup>a</sup> KMOS: multi-IFU at the VLT; SINFONI: single-IFU at the VLT; OSIRIS: single-IFU at Keck; NIFS: single-IFU at Gemini. Seeing-limited and adaptive optics-assisted surveys are distinguished (no-AO, AO).<sup>b</sup> Survey on-going or recently completed; band, on-source integration times, number of objects targeted, redshift range, and galaxy properties of detected subsets in Figure 3 and in fourth column refer to the published samples in the references given in the last column. <sup>c</sup> KLASS also targeted $z > 7$ galaxies.
SUPPLEMENTAL TEXT: SPECTRAL AND KINEMATIC MODELING

The past decade has seen important developments in modeling of the spectral energy distribution (SED) and kinematics data of distant galaxies, to derive their stellar populations properties such as stellar mass, age, star formation rate and history as well as their dynamical properties such as circular velocity and dynamical mass. Deriving these fundamental properties is essential to place observed galaxies in the theoretical framework of galaxy evolution through comparisons with (semi-)analytical models and numerical cosmological simulations. As spectral and kinematic data sets are growing rapidly in both sample size and detail of information, increasingly sophisticated approaches are being developed to improve the efficiency of modeling codes and treat adequately the various parameter correlations involved. Here we summarize basic ingredients and methods employed in state-of-the-art SED and kinematic modeling applied to data of high-redshift galaxies.

Spectral Modeling

The translation from SEDs to physical quantities describing a galaxy’s stellar mass, star formation rate or history requires the use of stellar population synthesis (SPS), dust, and ideally photoionization models. This is the case for SEDs sampled at any spectral resolution, and we therefore discuss these techniques indiscriminately of $R$.

The ingredients to SPS models include a stellar spectral library, a set of isochrones, an IMF, and a star formation history (SFH). Each of these components is discussed in depth in the review by Conroy (2013). Here we highlight a few succinct aspects of particular relevance to the study of distant galaxies. The stellar library is to cover a range in stellar metallicities, effective temperatures and surface gravities appropriate for the stellar population hosted by the galaxy under consideration. Since empirical libraries are composed from spectral observations of stars in the Solar neighborhood, they may lack or cover too sparsely certain regions of parameter space that potentially could contribute significantly to the integrated emission of early galaxies. In order to include very sub- or super-Solar metallicities, or stars caught during short-lived evolutionary phases such as Wolf-Rayet (WR) or thermally-pulsating asymptotic giant branch (TP-AGB) phases, theoretical libraries can be employed instead, even though these are not without flaws themselves, ranging from the treatment of convection to the quality and completeness of atomic and molecular line lists underpinning them. A hybrid approach has been applied as well, in which theoretically motivated differential corrections are applied to empirical spectra to provide a denser and more complete sampling of parameter space, e.g., in metallicity and elemental abundance (Conroy & van Dokkum 2012). Short-lived evolutionary phases also pose a challenge when pairing stellar libraries with isochrones to construct so-called single (i.e., mono-age) stellar populations. Approaches alternative to the “isochrone synthesis” technique have been explored by, e.g., Maraston (2005) who adopted the fuel consumption theorem in which the amount of hydrogen and/or helium consumed is taken as integration variable, in principle allowing luminous, short-lived evolutionary stages such as TP-AGB stars to be captured more fully. With substantial contributions to the rest-frame near-IR they were argued to significantly impact inferred galaxy stellar ages and masses, particularly at cosmic noon where characteristic stellar population ages match the phase where TP-AGB stars are most prominent ($\sim 3 \times 10^9 - 2 \times 10^9$ yr). That said, observational efforts at intermediate (Kriek et al. 2010) and higher spectral resolution (Zibetti et al. 2013) failed to find strong TP-AGB spectral signatures in those galaxies where they ought to be most prominent, potentially
explained by (self-produced) dust attenuating the TP-AGB light. An extensive review on the IMF, and evidence for potential deviations from the standard (Chabrier 2003) IMF, is presented by Hopkins et al. (2018). Claims of non-universality of the IMF based on observations of distant galaxies themselves (e.g., a top-heavy IMF in order to reconcile number counts of submillimeter galaxies with models (Baugh et al. 2005), or to reconcile a census of the cosmic SFR density and stellar mass assembly history (Wilkins et al. 2008)) are not unambiguous in their interpretation (see, e.g., Safarzadeh et al. 2017, Leja et al. 2019b). More convincing evidence, of a more bottom-heavy IMF in nearby ellipticals with high velocity dispersions, was provided based on three orthogonal lines of inquiry: IR spectroscopy (Conroy & van Dokkum 2012), dynamical modeling (Cappellari et al. 2013) and gravitational lensing (Treu et al. 2010). While the peak in SFH of these galaxies can be traced back to the cosmic noon era, an application of such IMF variations has yet to find its way into direct look-back studies, with as additional complication that the respective IMF changes may be confined to the central regions of these galaxies (Conroy et al. 2017).

Finally, SFGs are not well represented by single stellar populations, and need to be modeled with extended SFHs. Here, a common approach has originally been to parametrize the SFH by an exponentially declining, so-called τ model, largely because of its historical roots in SPS modeling of nearby early-type galaxies to which the technique was applied first. Renzini (2009) made the case that rising SFHs may be more appropriate for SFGs at cosmic noon, and hence more flexible functional forms (delayed τ models, log-normal SFHs, or double power laws) are increasingly being adopted. Offering yet more freedom, Pacifici et al. (2015) adopt a more extensive and physically motivated library of SFHs drawn from a semi-analytical model of galaxy formation, and conclude that a quantification of the normalization, slope and scatter of the stellar mass - SFR relation can be severely biased if both quantities are inferred from a common, oversimplified approach. In the same vein (Leja et al. 2019a) advocate the use of more flexible non-parametric (i.e., piecewise constant) star formation histories, and stress the importance of adopting appropriate priors.

Attenuation by dust, present in copious amounts within massive SFGs at cosmic noon, has a dimming and reddening effect on the emerging SED. With the exception of the potential presence of a bump at 2175 Å, often attributed to PAH molecules, its wavelength dependence is smooth, but nevertheless leaves a signature that is highly degenerate with variations in stellar age and/or metallicity. Whereas the most common approach is to adopt the Calzetti et al. (2000) reddening law calibrated locally on a sample of starbursting galaxies, in recent years first strides are made to map the attenuation curves at high z and their variation as a function of galaxy type directly (e.g., Kriek & Conroy 2013, Reddy et al. 2015). As an aid in breaking age-metallicity-dust degeneracies, SPS modeling codes increasingly are capable of accounting for far-IR constraints, where available. Any emission absorbed at short wavelengths should contribute to dust heating with associated reprocessed emission at long wavelengths. Several state-of-the-art SPS modeling codes such as MAGPHYS (da Cunha et al. 2015), BEAGLE (Chevallard & Charlot 2016), Prospector (Leja et al. 2017), and BAGPIPES (Carnall et al. 2018) now incorporate such energy balance arguments as well as Bayesian inference to explore parameter space. If not known spectroscopically, redshifts can be fit for simultaneously by these codes, enabling a self-consistent assessment of the error budget, including covariances.

As a third component besides the SPS and dust models, photoionization codes such as CLOUDY (Ferland et al. 2017) or MAPPINGS (Sutherland & Dopita 2017) can be employed to superpose on the stellar emission the anticipated nebular lines. This is indispensable
for full spectral fitting, but contributions from nebular line emission can also matter (and provided proper modeling even help) at lower spectral resolutions, especially when medium- or narrow-bands are included or for galaxies with high specific SFRs (e.g., van der Wel et al. 2011). Kewley et al. (2019) and Maiolino & Mannucci (2019) present comprehensive overviews of the ingredients to photoionization models and recent advances in their application and calibration to galaxies across cosmic time. The need for redshift-appropriate calibrations was brought to light by the observation of systematic shifts in the characteristic strong rest-optical line ratios captured in excitation diagrams, revealing the evolving ISM conditions (see Section 3.6) as well as the changing shapes of the ionizing radiation field. Topics of current debate in this regard entail, from a modeling perspective, the role attributed to stellar rotation, binary evolution, and stellar mass loss in determining the amount of ionizing photons and their hardness (e.g., Eldridge & Stanway 2012). SPS codes equipped with grids from photoionization models generally implement this in a self-consistent manner such that line intensities are tied to the metallicity and star formation history of the stellar population, but nevertheless the dimensionality of the problem is typically increased by the introduction of additional free parameters, such as the extra attenuation to HII regions.

Overall, it is well established that stellar mass represents the quantity on which SPS techniques can place the tightest constraints, as its inference requires an assessment of the mass-to-light (M/L) ratio only, to zeroth-order blind to the physical conditions responsible for setting this M/L (i.e., the balance of age, metallicity and dust attenuation). Whereas systematic differences arise depending on the assumptions made, code-by-code comparisons at various levels of control suggest that at least in terms of mass ranking a high degree of consistency is reached (Mobasher et al. 2015). SFRs can be more challenging in the presence of large columns of dust, in which case panchromatic information aids greatly. Star formation histories represent the most challenging inference in the case of SFGs.

Looking ahead, a few avenues can be identified for future progress in this area. First, with the increasing availability (and with the advent of JWST also wavelength coverage) of spatially resolved information, SPS modeling can be applied to SEDs extracted on sub-galactic scales. This has the merit of allowing to trace the stellar build-up in situ, but in addition can mitigate outshining effects. Whereas resolved SED modeling may go at the expense of wavelength coverage and sampling, galaxy-integrated constraints can be imposed (see, e.g., Wuyts et al. 2012). Second, in almost all applications to date a uniform metallicity is adopted for the entire stellar population. In future work, one could envision star formation and chemical enrichment histories to be coupled self-consistently, an approach that several of the aforementioned codes already allow for in principle. Exactly what constitutes a self-consistent treatment is an issue that may not be addressed trivially, as the connection between the two histories is modulated by gaseous in- and outflows, both of which are ubiquitous around cosmic noon. Finally, a full interpretation of galaxy spectra and emission lines would ideally account not only for full SPS but also for radiative transfer. Such full-fledged 3D radiative transfer modeling is to date restricted to a handful of very nearby galaxies for which very high-resolution datasets are available (e.g., De Looze et al. 2014). Much simplified analytical descriptions of absorption and scattering under different geometries such as homogeneous mixtures, (clumpy) foreground screens, and mixtures thereof can be applied via analytical recipes to interpret the distribution of line strengths and ratios resolved on kiloparsec scales within 100s of nearby galaxies (e.g., Li et al. 2019).
Kinematic Measurements and Modeling

To date, kinematics of distant star-forming galaxies come exclusively from observations of emission lines, mostly Hα or other rest-optical nebular lines, or CO transitions in the submillimeter regime. The best constraints are obtained from integral field unit (IFU) spectroscopy or interferometry, providing simultaneously the full three-dimensional (3D) data, which is the focus in what follows. Galaxy-integrated and slit spectra have been used to derive kinematic properties, and slit spectra were also modeled, following similar approaches as outlined below adapted for that type of data (e.g., Weiner et al. 2006, Price et al. 2016).

The data are usually interpreted in the framework of axisymmetric rotating disks motivated by the observations (Section 4 of the main article) where physical quantities of interest include for instance the intrinsic peak rotation velocity \( v_{\text{rot}} \) and local velocity dispersion \( \sigma_0 \), and the total dynamical mass of the system \( M_{\text{dyn}} \). Various approaches are followed, ranging from simple determinations based on the observed maximum velocity difference and line widths measured directly from the data or estimated by adjusting a parametric representation of the velocity curve and dispersion profile (e.g., computed for an exponential distribution, or approximated by an arctan function) to full forward modeling of the data. The simpler methods use one-dimensional (1D) major-axis profiles or 2D maps extracted from the data cubes. The flux, velocity, and dispersion are usually obtained by fitting the observed line emission with a single Gaussian, which was shown to be adequate for the typical resolved scales and S/N levels of high-z galaxy data (Förster Schreiber et al. 2018, Tiley et al. 2019). Deviations from a single Gaussian may become appreciable in galaxy-integrated spectra depending, for instance, on the spatial distribution of the tracer emission line, the local intrinsic gas velocity dispersion, and the possible presence of strong galactic-scale winds; these effects should be taken into account in estimating rotation velocities from galaxy-integrated line widths (e.g., de Blok & Walter 2014, Wisnioski et al. 2018). Spatial beam smearing, instrumental spectral resolution, and galaxy inclination \( i \) are treated explicitly by rescaling of the observed maximum velocity and local dispersion through functions or lookup tables based on mock beam-smeared rotating disk models parametrized in terms of \( R_{\text{beam}}/R_e \) and galaxy properties (such as mass and inclination for \( \sigma_0 \)), by subtracting in quadrature the instrumental broadening from the measured dispersion, and by dividing the projected velocity by \( \sin(i) \) derived from the morphology (e.g., Burkert et al. 2016, Johnson et al. 2018). Studies applying forward modeling perform fits of 1D profiles, 2D maps, or

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10For an exponential model, the maximum velocity is reached at a radius \( R_{\text{max}} = 2.2 R_d = 1.3 R_e \), where \( R_d \) is the disk scale length and \( R_e \) the effective radius enclosing half the light, in which case measuring a \( v_{2.2} \) at 2.2 \( R_d \) is the same as \( v_{\text{rot}} \). The choice between \( v_{\text{rot}} \) and \( v_{2.2} \) depends on the goal of the analysis. Deviations from an exponential distribution change the \( R_{\text{max}}/R_e \) (Binney & Tremaine 2008), such that measuring the maximum \( v_{\text{rot}} \) is ideally done from the velocity curve rather than at fixed radius. The quantity \( \sigma_0 \) refers to the velocity dispersion across the galaxy as a measure of “turbulence,” which, in the case of a disk and isotropic dispersion, is related to its geometrical thickness. It is to be distinguished from the total velocity dispersion \( \sigma_{\text{tot}} \) measured from the line width in source-integrated spectra (which includes line broadening from galaxy-wide velocity gradients) and from the central velocity dispersion commonly employed in the analysis of early-type systems (which would be strongly dominated by beam-smearing of the steep inner velocity gradient for a disk). To minimize line broadening caused by inner disk velocity gradients, \( \sigma_0 \) is best measured away from the central regions. In data of high-z galaxies, \( \sigma_0 \) may also include contributions by noncircular motions on scales below the resolution element (\( \lesssim 1−5 \) kpc depending on data set).
3D cubes. The effects of resolution and inclination are treated implicitly by convolving the intrinsic, inclined 3D model with a kernel representing the point and line spread functions (PSF and LSF; e.g., Cresci et al. 2009, di Teodoro & Fraternali 2015).

Kinematic modeling codes developed specifically for application to observations at high redshift have become increasingly sophisticated in recent years to allow more flexibility in model assumptions, more efficient parameter space exploration, and better quantification of uncertainties of the best-fit values accounting for covariances. Examples include the DYSMAL code (e.g., Davies et al. 2011, with recent updates described by Wuyts et al. 2016, Ubler et al. 2018, Genzel et al. 2020), GalPaK3D (Bouché et al. 2015), and 3D-BAROLO (di Teodoro & Fraternali 2015), all based on axisymmetric models but differing in ingredients and dimensional space in which fits are performed. The most recent version of DYSMAL allows to fit multiple mass components, such as a disk and a bulge, with relative mass ratios specified and parametrized as Sérsic profiles; the code self-consistently accounts for finite thickness (turbulent disk, flattened rotating bulge) based on Noordermeer (2008). The baryonic component(s) can be embedded in a dark matter halo with a choice of profile parametrizations (e.g., “NFW,” Navarro et al. 1996, double power-law; cored Burkert 1995 profile). The line-of-sight velocity distribution is computed from the total mass model and relative weights can be applied to the light of different components. DYSMAL is optimized to fit in 1D or 2D although 3D fitting also is possible. GalPaK3D is designed to fit simultaneously structural and kinematic parameters directly in 3D data cubes, assuming a light/mass component among several choices (e.g., exponential, Gaussian, and de Vaucouleurs profiles), different parametrizations of the velocity profile (e.g., arctan, inverted exponential, hyperbolic, or computed from the 3D mass model). Both DYSMAL and GalPaK3D employ Markov chain Monte Carlo (MCMC) algorithms in a Bayesian framework to derive the best-fit parameters and uncertainties thereof. 3D-BAROLO fits tilted ring models to 3D data, where each concentric ring is parametrized independently and is randomly populated with line emitting clouds in six dimensions (three in each of spatial and velocity space), from which line profiles are built and projected into the model cube. This method can more naturally account for possible variations in orbits with radius, such as warps. The code uses a multidimensional downhill simplex solver for the minimization of non-analytic models, with uncertainties estimated via a Monte Carlo method.

In principle, fitting in 3D space offers a number of advantages as it avoids the necessary loss of information in extracting the projected 2D maps or 1D profile from both data and model. In practice, the success of the fits can be hampered by low S/N and irregular or clumpy light distributions. For axisymmetric mass distributions, most of the information is encoded along the line of nodes, such that the parameters can be well determined from 1D fits; for sufficiently high S/N and well resolved galaxies, 2D maps can constrain more accurately the inclination. Especially at high redshift, the morphology in line emission can be quite different from the underlying mass distribution and cannot be captured by simple representations, let alone in 3D (which ideally would best account for projection and light weighting effects); in such cases, fits are best performed only in velocity and dispersion. Despite the flexibility afforded by the above models, the observations may not allow to constrain well all possible parameters but the implementation of Bayesian analysis and MCMC algorithms have brought a major improvement over previous modeling by allowing for priors and propagation of uncertainties including covariances rather than simply fixing values.

The residuals between observed data and best-fit kinematic model can be used in implementing the kinematic classification scheme discussed in Section 4.3. An alternative
classification method relies on kinemetry, introduced by Krajnović et al. (2006) to analyze data of nearby early-type galaxies and adapted for applications to IFU studies of distant SFGs by Shapiro et al. (2008). Kinemetry is a generalization of surface photometry to the higher-order moments of the line-of-sight distribution, where the degree of (a)symmetry in the velocity field and dispersion map along best-fit ellipses is quantified through harmonic expansions. The exact values of the parameters will depend on the resolution and S/N regime of the data, such that the boundaries to distinguish between disks and mergers need to be appropriately calibrated for the data sets under analysis.

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