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Pressure dependence of ferromagnetic phase boundary in BaVSe$_3$ studied with high-pressure $\mu^+\text{SR}$

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The magnetic nature of a quasi-one-dimensional compound, BaVSe$_3$, has been investigated with positive muon spin rotation and relaxation ($\mu^+\text{SR}$) measurements at ambient and high pressures. At ambient pressure, the $\mu^+\text{SR}$ spectrum recorded under zero external magnetic field exhibited a clear oscillation below the Curie temperature ($T_C \sim 41$ K) due to the formation of quasistatic ferromagnetic order. The oscillation consisted of two different muon spin precession signals, indicating the presence of two magnetically different muon sites in the lattice. However, the two precession frequencies, which correspond to the internal magnetic fields at the two muon sites, could not be adequately explained with relatively simple ferromagnetic structures using the muon sites predicted by density functional theory calculations. The detailed analysis of the internal magnetic field suggested that the V moments align ferromagnetically along the $c$ axis but slightly canted toward the $a$ axis by 28$^\circ$ that is coupled antiferromagnetically. The ordered V moment ($M_V$) is estimated as (0.59, 0, 1.11) $\mu_B$. As pressure increased from ambient pressure, $T_C$ was found to decrease slightly up to about 1.5 GPa, at which point $T_C$ started to increase rapidly with the further increase of the pressure. Based on a strong ferromagnetic interaction along the $c$ axis, the high-pressure $\mu^+\text{SR}$ result revealed that there are two magnetic interactions in the $ab$ plane; one is an antiferromagnetic interaction that is enhanced with pressure, mainly at pressures below 1.5 GPa, while the other is a ferromagnetic interaction that becomes predominant at pressures above 1.5 GPa.

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I. INTRODUCTION

In the quasi-one-dimensional (Q1D) triangular compound, in which the 1D ferromagnetic (FM) interaction along the $c$ axis is stronger than the two-dimensional (2D) FM and/or antiferromagnetic (AF) interactions in the $ab$ plane, the magnetic ground state is naturally determined by the competition between the 2D-FM and 2D-AF interactions. When the 1D FM chains form a 2D triangular lattice (2DTL) with $S = \frac{1}{2}$, geometrical frustration provides further complexity in determining the magnetic ground state [1]. Since the delicate balance of the multiple 2D interactions in such a Q1D-2DTL system is expected to be affected by tuning the interchain distances with pressure, the magnetic phases could also drastically depend on pressure. To study the magnetic nature of the Q1D-2DTL system, a positive muon spin rotation and relaxation ($\mu^+\text{SR}$) experiment was initiated, since $\mu^+\text{SR}$ is one of the most powerful tools for studying internal magnetic fields in solids at both ambient and high pressures due to its unique spatial and time resolutions [2,3]. In fact, the recent ambient and high-pressure $\mu^+\text{SR}$ work on a Q1D-2DTL compound, BaVS$_3$ [4], which is known to exhibit a metal-insulator transition at $T_M = 70$ K driven by the formation of a commensurate charge density wave (CDW) Peierls ground state [5–10], has clarified that BaVS$_3$ enters a linear incommensurate spin density wave ordered state below the Néel temperature ($T_N$) 31 K at ambient pressure [4,11]. Furthermore, $T_N$ is almost constant as the pressure ($p$) increases from ambient pressure to 1.4 GPa, then $T_N$ decreases rapidly for $p > 1.4$ GPa, and finally disappears at $p \sim 1.8$ GPa [4], above which a metallic phase is stabilized. Hence, combining the pressure dependence of $T_M$ [12–15], $T_N$ is found to coincide with $T_M$ at $p > 1.4$ GPa [4].

Despite a glamorous electronic and magnetic phase diagram in BaVS$_3$, there are a limited number of experiments on the isostructural compound BaVSe$_3$ [17–22]. BaVSe$_3$...
undergoes a structural phase transition from a high-temperature hexagonal phase with space group \( P6_3/mmc \) to a low-temperature orthorhombic phase with space group \( Cmc2_1 \) at \( T_\text{C} = 310 \text{ K} \) [17,18] (Fig. 1). BaVSe\(_3\) exhibits a paramagnetic metallic behavior at high temperatures and enters an FM metallic phase below the Curie temperature \( (T_\text{C}) \) at 43 K [18,19]. Magnetization and torque measurements on a single crystal revealed that the easy magnetization axis in the FM phase is parallel to the chain direction, i.e., the \( c \) axis, the one-dimensional (1D) V chain along the \( b \) axis, the one-dimensional (1D) V chain along the \( b \) axis. The three muon sites predicted by density functional theory (DFT) calculations are drawn with small yellow, blue, and pink spheres at \( \mu_1 (0, 0.35, 0.25) \), \( \mu_2 (0, 0.44, 0.225) \), and \( \mu_3 (0.33, 0.33, 0) \), respectively.

II. EXPERIMENTAL

A powder sample of BaVSe\(_3\) was prepared by a conventional solid state reaction technique reported in Ref. [19]. A mixture of BaSe, VSe\(_2\), and Se with a molar ratio of 1:1:0.1 was heated in an evacuated quartz tube at 1223 K for 100 h. The sample was characterized by powder x-ray diffraction analysis and magnetization measurements with a superconducting quantum interference device magnetometer (MPMS, Quantum Design), as seen in Fig. 2.

The \( \mu^+ \)SR spectra of BaVSe\(_3\) were recorded using both the General Purpose Spectrometer (GPS) at the surface muon beamline p\( \mu \)M3 and the General Purpose Decay-Channel Spectrometer (GPD) at the decay beamline \( \mu \)E1 of the Laboratory for Muon Spin Spectroscopy (LMU) of the Paul Scherrer Institute (PSI) in Switzerland. On GPS, approximately 200 mg of powder sample was placed in an envelope with \( 1 \times 1 \text{ cm}^2 \) area, made of Al-coated Mylar tape with 0.05 mm thickness to minimize the signal from the envelope. The envelope was attached to a fork-type low-background sample holder and inserted in a liquid-He flow-type cryostat for measurements in the temperature range between 1.6 and 70 K.

On GPD, three pelletized discs of the powder sample with 6 mm diameter and 15 mm total height (5 mm each) were stacked in a piston-cylinder-type pressure cell made of MP35N alloy. To apply hydrostatic pressure to the sample, Daphne oil was used as a pressure transmitting medium. The actual pressure at low temperatures was estimated by measuring the superconducting transition temperature of an indium wire placed at the bottom of the sample space, by alternating current susceptibility. The accuracy of the pressure determined by such a measurement is estimated as \( \pm 0.01 \text{ GPa} \).
A Janis $^4$He flow cryostat was used to reach temperatures as low as 2 K.

The $\mu^+\text{SR}$ time spectra were recorded at temperatures between 1.6 and 70 K under zero field (ZF) and externally applied magnetic field, namely, weak transverse field (wTF) and longitudinal field (LF). Here, TF [LF] means the field applied perpendicular [parallel] to the initial $\mu^+$ spin polarization, and “weak” means that the field is very small (50 Oe, this time) compared with the internal FM field. The experimental techniques are described in more detail elsewhere [2,3,4,25]. The obtained $\mu^+\text{SR}$ data were analyzed with the MUSRFIT software suite [26].

The muon sites and local spin density at each muon site in the BaVSe$_3$ lattice were predicted by density functional theory (DFT) calculations using a full-potential linearized augmented plane-wave method within generalized gradient approximations as implemented in WIEN2k program package [27]. In the calculations, the lattice parameters and atomic positions of BaVSe$_3$ were taken from Ref. [22]. The magnetic moments were aligned parallel to the $c$ axis through spin-orbit coupling. The muffin tin potential radii ($R_{\text{MT}}$) for Ba, V, and Se were taken to be 1.32, 1.20, and 1.06 Å, respectively. The energy cutoff was chosen to be $R_{\text{MT}} \times K_{\text{max}} = 7.0$, and $11 \times 11 \times 11$ $k$-points meshes were used in the Brillouin zone. Here, $K_{\text{max}}$ is the maximum modulus for the reciprocal vectors. Such predictions reveal that there are three possible muon sites in the lattice: (0, 0.35, 0.25), (0, 0.44, 0.225), and (0.33, 0.33, 0) (see Fig. 1), defined according to the local Coulomb potential minima.

III. RESULTS

A. wTF-$\mu^+\text{SR}$ at ambient pressure

To confirm the sample quality and determine $T_C$, and the transition width ($\Delta T_C$), the $\mu^+\text{SR}$ spectrum was measured in a wTF. Figure 3(a) shows wTF-$\mu^+\text{SR}$ spectra recorded below and above $T_C$. The muon spin precesses around wTF with a full asymmetry in a paramagnetic phase, whereas with a zero asymmetry in a magnetically ordered phase when the internal magnetic field is very large compared with wTF. The wTF asymmetry ($A_{\text{TF}}$) is therefore roughly proportional to the volume fraction of the paramagnetic phases in the sample. In fact, the wTF-$\mu^+\text{SR}$ spectrum exhibits a clear oscillation without relaxation at 60.5 K. Such amplitude, i.e., $A_{\text{TF}}$ decreases with decreasing temperature from 43.4 K and becomes invisible at 39.3 K. Considering the presence of the precession signal due to the FM internal magnetic field in the early time domain below $T_C$ (see Sec. III B), the wTF-$\mu^+\text{SR}$ spectrum was fitted in a time domain between 0.3 and 10 $\mu$s with the exponential decay rate ($\lambda_{\text{TF}}$) and a steplike change in the $\mu^+\text{SR}$ signal. As temperature decreases from 60 K, the $A_{\text{TF}}/A_0$ curve exhibits a steplike change at around 40 K, while both $A_{\text{TF}}$ and $A_0$ appear below 30 K. From the middle point of the steplike change in the $A_{\text{TF}}/A_0$ curve, $T_C$ and $\Delta T_C$ are determined as 40.82(12) K and 0.69(14) K, respectively, using a Sigmoid function. The $\lambda_{\text{TF}}$ curve shows a clear maximum at around $T_C$, as a critical behavior of the magnetic transition. These results indicate that the sample is a single phase, i.e., no detectable impurity phase within the $\mu^+\text{SR}$ sensitivity, and the whole sample enters an FM phase below $T_C$.

B. ZF-$\mu^+\text{SR}$ at ambient pressure

Figure 4 shows the ZF-$\mu^+\text{SR}$ time spectrum for BaVSe$_3$ recorded at the lowest temperature measured (1.6 K). Since the spectrum exhibits a clear oscillation with almost full amplitude ($\sim 0.25$), the whole volume of the sample is found to enter a FM ordered state. Furthermore, a complex time structure of the ZF spectrum indicates the presence of multiple components with different oscillatory frequencies. In fact, the Fourier transform of the time spectrum indicates the presence of two different frequency components [Fig. 4(b)], suggesting...
FIG. 4. (a) The zero field (ZF)-\(\mu^+\)SR time spectrum for BaVSe\(_3\) recorded at 1.6 K, and (b) the Fourier transform power spectrum of (a). In (a), a solid line represents a best fit with Eq. (2). In (b), two arrows represent the muon spin precession frequencies obtained by fitting the ZF-\(\mu^+\)SR time spectrum with Eq. (2).

the existence of two magnetically different muon sites in the BaVSe\(_3\) lattice.

Considering the internal magnetic field distribution in both a FM phase and a paramagnetic phase, the \(\mu^+\)SR time spectrum was fitted by a combination of two exponentially relaxing cosine functions, an exponentially relaxing nonoscillatory signal for a \(1/3\) tail signal in a powder sample \([2,3]\), and a Gaussian Kubo-Toyabe signal for the sample in a paramagnetic state:

\[
A_0 P_{ZF}(t) = A_{FM1} \cos(2\pi f_{FM1}t) \exp(-\lambda_{FM1}t) + A_{FM2} \cos(2\pi f_{FM2}t) \exp(-\lambda_{FM2}t) + A_{tail} \exp(-\lambda_{tail}t) + A_{KT} G_{KT}^{zz},
\]  

(2)

where \(A_0\) is the initial asymmetry, \(A_{FM1}, A_{FM2}, A_{tail},\) and \(A_{KT}\) are the asymmetries associated with the four signals, \(f_{FM1}\) and \(f_{FM2}\) are the muon Larmor frequencies corresponding to the quasistatic internal FM fields, \(\lambda_{FM1}, \lambda_{FM2},\) and \(\lambda_{tail}\) are their exponential relaxation rates. Here, \(G_{KT}^{zz}\) is a static Gaussian Kubo-Toyabe function and given by \([28]\)

\[
G_{KT}^{zz}(t, \Delta) = \frac{1}{3} + \frac{2}{3}(1 - \Delta^2 r^2) \exp \left( -\frac{1}{3} \Delta^2 t^2 \right),
\]  

(3)

where \(\Delta\) is related to the width of the magnetic field distribution at the muon site in the paramagnetic state. To use the same fit function for the ZF-\(\mu^+\)SR spectra in the whole temperature range, we have set \(f_{FM1} = f_{FM2} = 0\) for \(T \geq T_c\), and \(A_{KT} = 0\) for \(T < T_c\). Furthermore, below \(T_c\), the asymmetries in the FM phase were fixed as follows: \((A_{FM1} + A_{FM2}) = \frac{2}{3} A_0\) and \(A_{tail} = \frac{1}{3} A_0\), where \(A_0 = 0.2455\) was estimated from the wTF-\(\mu^+\)SR measurements at 60 K, which is well above \(T_c\).

Figure 5 shows the temperature dependencies of the \(\mu^+\)SR parameters in BaVSe\(_3\) at ambient pressure. (a) The two muon spin precession frequencies \((f_{FM1} \text{ and } f_{FM2})\), (b) the ratio between \(f_{FM1} \text{ and } f_{FM2}\) \((f_{FM1}/f_{FM2})\), (c) the asymmetries \((A_{FM1}, A_{FM2}, A_{tail}, \text{ and } A_{KT})\), (d) the exponential relaxation rates of \(A_{FM}\) signals \((\lambda_{FM1} \text{ and } \lambda_{FM2})\), and (e) the exponential relaxation rate of the tail signal \((\lambda_{tail})\) and the field distribution width \((\Delta)\). The data were obtained by fitting the ZF-\(\mu^+\)SR spectrum with Eqs. (2) and (3). Vertical broken lines show the Curie temperature determined by weak transverse field (wTF) measurements (see Fig. 3); that is, \(T_c = 40.74(8) \text{ K}\). In (a) and (b), error bars are smaller than the data point symbols. In (d), \(\Delta(ZLF)\) represents \(\Delta\) obtained by fitting the ZF- and longitudinal field (LF)-\(\mu^+\)SR spectra simultaneously using a common \(\Delta\) for \(T < T_c\)
temperature and disappears at $T_C$. Below $T_C$, but above 39 K, the FM2 signal merges with the FM1 signal. The precession frequency- vs-temperature curve usually corresponds to the temperature dependence of the order parameter of a magnetic transition. In fact, since the ratio between the two oscillation frequencies ($f_{\text{FM1}}/f_{\text{FM2}} \sim 1.352$ at 1.6 K) is almost temperature independent up to below the vicinity of $T_C$, it is reasonable to assert that both $f_{\text{FM1}}$ and $f_{\text{FM2}}$ come from the internal magnetic field originated from the same FM phase in BaVSe$_3$ but from two uniquely magnetically different muon sites. Overall, the obtained result clearly indicates that the two oscillatory signals are not caused by the presence of multiple different magnetic phases in the sample, but are caused by the presence of multiple different muon sites in the BaVSe$_3$ lattice. Such an assertion is also supported by the wTF measurements presented above. In FM materials, the internal magnetic field at the muon site ($\textbf{H}_\mu$) is not solely composed of dipolar fields ($\textbf{H}_{\text{dip}}$) formed by FM ordered moments. This will be discussed in Sec. IV A.

As temperature increases from 2 K, $A_{\text{FM1}}$ [$A_{\text{FM2}}$] slightly increases [decreases] up to about 10 K, then decreases [increases] up to about 30 K, and shows a complex temperature dependence around $T_C$. Although $A_{\text{tail}}$ is fixed at $\frac{4}{3}A_0 = 0.08183$ up to about 40 K, $A_{\text{tail}}$ decreases with further increasing temperature above $T_C$, and disappears around 50 K. Instead, $A_{\text{KT}}$ increases with temperature above $T_C$ and levels off to a maximum value at $T \geq 50$ K, meaning that the whole volume of the BaVSe$_3$ sample is in a paramagnetic state.

Both $\lambda_{\text{FM1}}$ and $\lambda_{\text{FM2}}$ are roughly temperature independent at $T < 35$ K. As temperature increases from 35 K, $\lambda_{\text{FM1}}$ increases with temperature toward $T_C$ and reaches a maximum slightly above $T_C$. On the contrary, $\lambda_{\text{FM2}}$ gradually decreases with increasing temperature from 35 K, and disappears around $T_C$, since the FM2 signal merges into the FM1 signal.

For the tail signal, which corresponds to the parallel component of the internal magnetic fields with respect to the initial muon spin polarization, $\lambda_{\text{tail}}$ is very small compared with $\lambda_{\text{FM}}$ at temperatures below 40 K and is almost temperature independent. However, $\lambda_{\text{tail}}$ increases with temperature close to $T_C$ and reaches a maximum at around 43 K, $\lambda_{\text{FM1}}$.

Since $\Delta$ is caused by nuclear magnetic moments of Ba, V, and Se, $\Delta$ is naturally negligible below $T_C$ compared with a large FM field in the lattice. The value of $\Delta$ is around 0.1 $\mu$s$^{-1}$, which corresponds to about 1.2 Oe, and slightly decreases with temperature, as expected. Using the observed $\Delta$ ($\Delta^{\text{obs}}$), the possible muon sites are further discussed in Sec. IV A.

C. $\mu^+\text{SR}$ at high pressures

For the $\mu^+\text{SR}$ measurements at high pressures, the BaVSe$_3$ discs with 6 mm diameter were set inside a pressure cell with an external diameter of about 26 mm. Hence, about 65% of the implanted muons stop in the pressure cell, and the rest (about 35%) stop in the sample. Since the pressure cell is paramagnetic even at the lowest temperature achievable on GPD, the muons stopped in the pressure cell provide an oscillatory signal due to wTF regardless of temperature. As a result, the normalized asymmetry [$A_{\text{TF}}(T)/A_0$] is unity at temperatures above $T_C$, while $A_{\text{TF}}(T)/A_0 \sim 0.65$ at temperatures below $T_C$. Although the change in $A_{\text{TF}}(T)/A_0$ at $T_C$ ($\sim 0.35$) is smaller than that without pressure cell ($\sim 1$), the wTF-$\mu^+\text{SR}$ measurements with temperature clearly provide $T_C$ even in the pressure cell.

Figure 6 shows the temperature dependence of $A_{\text{TF}}(T)/A_0$ for several pressures together with the result obtained without the pressure cell in the same temperature range, for comparison. The wTF-$\mu^+\text{SR}$ spectrum in the pressure cell was also fitted by Eq. (2). At each pressure, the $A_{\text{TF}}(T)/A_0$ curve exhibits a steplike change at around 41 K, as in the case without the pressure cell [Fig. 6(c)]. From the middle point of the steplike change in the $A_{\text{TF}}(T)/A_0$ curve, $T_C$ is estimated as 41.2(2) K at 0.1 MPa, which is roughly equivalent to the value estimated from the wTF data obtained without the pressure cell within the estimation accuracy [40.82(12) K]. As pressure...
were obtained by fitting the spin precession frequencies at 5.5 K for BaVSe$_3$. The former data were obtained from the muons stopped in the pressure cell and not the internal magnetic field at the muon sites. More precisely, $f_{FM1}$ increases with $p$ monotonically up to around 2 GPa and then looks to level off to a constant value at around 17 MHz. On the contrary, $f_{FM2}$ slowly increases with $p$ up to around 1.5 GPa and then increases more rapidly with $p$ up to 2.35 GPa. Considering the fact that $A_{FM1} > A_{FM2}$ below 10 K [see Fig. 5(b)], the $f_{FM1}(p)$ curve is more reliable than the $f_{FM2}(p)$ curve. Hence, the internal magnetic fields at the muon sites are found to increase monotonically with $p$.

IV. DISCUSSION

A. Internal magnetic field at ambient pressure

Before discussing the FM spin structure of BaVSe$_3$, the possible muon sites based on the $\mu^+\text{SR}$ result in the paramagnetic state is considered using the observed $\Delta$ ($\Delta_{obs}$). Since the value of $\Delta$ at 0 K ($\Delta_{calc}$) is predicted with the dipole field calculations (nuclear dipoles), the inequality $\Delta_{obs} \leq \Delta_{calc}$ is valid in the presence of any dynamics at nonzero temperatures. In fact, back to the related compound BaVS$_3$, $\Delta_{obs} = 0.725$ Oe at 43 K, while $\Delta_{calc} = 0.940$ Oe for the first site at ($\frac{1}{2}$, $\frac{1}{2}$, $\frac{1}{2}$) and 2.319 Oe for the second site at ($\frac{1}{2}$, $\frac{1}{2}$, $\frac{1}{2}$). Since the asymmetry of the signal from the first site is comparable with that from the second site [4], $\Delta_{obs}$ is found to be about a half of the prediction $(0.725 : \frac{2.319}{2} = 0.44 : 1)$.

For BaVSe$_3$, $\Delta_{obs} = 0.1 \mu$s$^{-1}$, which corresponds to 1.2 Oe, at 50 K [see Fig. 5(d)]. Hence, the scenario that the implanted muons locate only $\mu_1$ ($\Delta_{calc} = 0.877$ Oe) and $\mu_2$ ($\Delta_{calc} = 0.977$ Oe) is highly unlikely given the $\Delta_{obs} = 1.2$ Oe. If we assume a similar reduction of $\Delta_{obs}$ to that in BaVS$_3$, i.e., $\Delta_{obs}$ at 0 K is assumed to be about 2.4 Oe for BaVSe$_3$, a certain portion of the implanted muons should locate $\mu_3$ ($\Delta_{calc} = 2.65$ Oe). This restricts the determination of the FM spin structure using the $\mu^+\text{SR}$ results.

For nonmagnetized FM materials in applied ZF, the internal magnetic field at a muon site ($H_{\mu}$) is represented by [3,29–32]

$$ H_{\text{FM}} = H_{\text{dip}} + H_{L} + H_{\text{hf}}, $$

where $H_{\text{dip}}$ is the dipolar field, $H_{L}$ is the Lorentz field, $H_{\text{hf}}$ is the hyperfine field. Furthermore, $H_{L}$ and $H_{\text{hf}}$ are connected to the saturated magnetization ($M_s$) and the local spin density at the muon sites ($\rho_{\text{spin}}$) as follows:

$$ H_{\text{dip}} = -\frac{1}{4\pi\mu_0} \nabla \left( \frac{m \cdot r}{r^3} \right), $$

$$ H_{L} = \frac{4\pi}{3} \times M_s, $$

$$ H_{\text{hf}} = \frac{8\pi}{3} \times \rho_{\text{spin}}(r) \times \frac{H_{\text{dip}}}{|H_{\text{dip}}|}. $$

To estimate $H_{\text{dip}}$, we use the results of magnetization measurements for the magnitude and direction of the V moments. That is, the magnitude of the ordered V moment ($M_V$) is 0.34 $\mu_B$ along the c axis [19], which is equivalent to $M_s$ at 2 K. Here, $H_{\text{dip}}$ at the muon site is then easily calculated with DIPELEC [33] using the crystal structural data.

Assuming a FM ordering along the c axis ((0,0,FM)) with $M_V = M_{Vc} = 0.34 \mu_B$, the predicted $H_{\text{dip}}$, $H_{L}$, and $H_{\text{hf}}$ are summarized in Table I. It is very clear that the predicted...
internal magnetic field \(H_{dip}\) at each muon site is too small to explain the experimental result. If we further assume \(M_V = M_{Vz} = 0.6(2) \mu_B\) based on the magnetization measurements for a single crystal sample [20], the predicted \(H_\mu(f_\mu)\) are still too small to explain the experimental result [see Fig. 8(a)]. In fact, the predicted \(f_\mu\) and \(f_{\mu2}\) are about 6% and 16% of the measured \(f_{\mu2}\) at 1.6 K even if \(M_{Vz} = 1 \mu_B\), although \(f_\mu\) is about 60% of \(f_{\mu2}\) at 1.6 K.

Therefore, we have attempted to introduce an AF component in the \(ab\) plane so as to avoid geometrical frustration. Here, the ordered V moment \(M_V\) is represented by \(M_{Vx}, M_{Vy}, M_{Vz}\). Back to Fig. 1, [0,AF,FM] means that V moments align parallel along the \(b\) axis but antiparallel between the neighboring V ions along the \(c\) axis, while [AF,0,FM] means that V moments align parallel along the \(a\) axis but antiparallel between the neighboring V ions along the \(b\) axis. For both [0,AF,FM] and [AF,0,FM], V moments align parallel along the \(c\) axis. Here, [AF,AF,FM] is a combination of [0,AF,FM] and [AF,0,FM]. The direction and magnitude of \(M_V\) are [011] and [011] for [0,AF,FM], [101] and [101] for [AF,0,FM], and [111] and [111] for [AF,AF,FM] with \(M_{Vz} = 0.34 \mu_B\). More correctly, \((M_{Vx}, M_{Vy}, M_{Vz}) = (0, 0.70, 0.34) \mu_B\) for [011], and \((0.41, 0.70, 0.34) \mu_B\) for [111], because \(a = 6.992(2) \AA, b = 12.113(3) \AA, c = 5.859(1) \AA\) [17]. The canting angle of the ordered V moments for [0,AF,FM] is 64° along the \(b\) axis \((\alpha)\), for [AF,0,FM] is 50° along the \(a\) axis \((\beta)\), and for [AF,AF,FM] is 67° along the [110] direction. Furthermore, for [AF,0,FM] and [AF,AF,FM], the \(\mu_3\) site is no longer magnetically equivalent, but splits into two magnetically different sites \((\mu_31\) and \(\mu_32\)). That is, among the eight equivalent \(\mu_3\) sites per unit cell in a paramagnetic state, four sites become the \(\mu_31\) site, and the rest become the \(\mu_32\) site below \(T_C\).

Figures 8(b)–8(d) show the relationship between \(M_{Vz}\) and the predicted internal magnetic field \(H_\mu(f_\mu)\) for [0,AF,FM], [AF,0,FM], and [AF,AF,FM]. The [0,AF,FM] model is clearly excluded because both \(f_{\mu2}\) and \(f_\mu\) are too small to explain \(f_{\mu2}\) in the whole \(M_{Vz}\) range between 0 and 1.1 \(\mu_B\). Considering the fact that \(A_{\mu1} > A_{\mu2}\) [see Fig. 5(b)], the [AF,AF,FM] model is also excluded. This is because the population of the muons at the \(\mu_31\) site is the same to that at the \(\mu_32\) site, resulting in \(A_{\mu1} = A_{\mu2}\). When the muons at the \(\mu_2\) site also contribute to the lower \(f_\mu\) signal, i.e., the \(f_{\mu2}\) signal, \(A_{\mu1} < A_{\mu2}\), being inconsistent with the experimental result.

To reproduce the ratio between \(f_{\mu1}\) and \(f_{\mu2}\), Fig. 9(a) shows the relationship between \(f_{\mu3}\) and \(f_{\mu2}\), i.e., \(f_{\mu3} + f_{\mu2} = f_{\mu1}\), and the canting angle toward the \(a\) axis \((\beta)\) for [AF,0,FM]. As \(M_{Vz}\) increases from 0.34 to 1.13 \(\mu_B\), the interaction between the \(f_{\mu3} + f_{\mu2}\) \((\beta)\) curve and the observed \(f_{\mu1}/f_{\mu2} (=1.352)\) shifts toward a higher \(\beta\) side. Moreover, when \(f_{\mu3}/f_{\mu2} = 1.352\), the predicted \(f_{\mu2}\) increases monotonically with \(M_{Vz}\), as seen in Fig. 9(c). To explain the observed \(f_{\mu2} (= 9.75 \text{ MHz})\) and \(f_{\mu1}/f_{\mu2} (=1.352)\), we obtain that \(\beta = 28°\) and \(M_{Vz} = 1.11 \mu_B\) \((M_{Vz} = 0.59 \mu_B)\), which is comparable with the magnetization measurement results for a single-crystal sample \((M_{Vz} = 0.62(2) \mu_B)\) [20] and the previous DFT calculation results \((M_{Vz} = 0.82 \mu_B)\) [21]. The total ordered moment is thus obtained as \(M_V = \sqrt{M_{Vx}^2 + M_{Vy}^2} = 1.26 \mu_B\).
FIG. 8. The relationship between the magnitude of the ordered V moment along the c axis ($M_{Vz}$) and the predicted internal magnetic field ($H_μ$ and $f_μ$) at the three muon sites for the ferromagnetic (FM) order (a) along the c axis ([0,0,FM]), (b) along the c axis but antiferromagnetic (AF) along the b axis ([0,AF,FM]), (c) along the c axis but AF along the a axis ([AF,0,FM]), and (d) along the c axis but AF along the a and b axes ([AF,AF,FM]). $f_{FM1}$ and $f_{FM2}$ correspond to the measured values obtained at 1.6 K. Here, we assumed that $M_{s,z} = M_{Vz}$. Two vertical broken lines show the previously reported $M_{Vz}$ ($= 0.32 \mu_B$ and $0.68 \mu_B$) by magnetization measurements [19,20].

On the contrary, for the [0,AF,FM] model, the intersection between the $f_{μ3}/f_{μ2}$ and the canting angle for (a) the [AF,0,FM] model and (b) the [0,AF,FM] model. In (a), the ordered V moment along the c axis ($M_{Vz}$) is changed from 0.34 to 1.13 $\mu_B$, $f_{μ3}/f_{μ2} = \frac{f_{μ3} + f_{μ2}}{2f_{μ2}}$, and the canting angle toward the a axis ($β$). In (b), $M_{Vz}$ is changed from 0.05 to 0.34 $\mu_B$ and the canting angle toward the b axis ($α$). (c) $f_{μ2}$ as a function of $M_{Vz}$, when $f_{μ3}/f_{μ2} = 1.352$. For [0,AF,FM], only $M_{Vz} \leq 0.19 \mu_B$ satisfies $f_{μ3}/f_{μ2} = 1.352$.

B. Internal magnetic field at high pressures

Comparing with the previous $μ^+\text{SR}$ work on an incommensurate AF (IC-AF) BaVS$_3$ (Fig. 10) [4], the distribution of the internal magnetic field in BaVSe$_3$ is like that in BaVS$_3$, except for the broad maximum around 20 MHz in BaVS$_3$ due to a wide field distribution caused by the IC-AF order [2–4,34]. This also supports that the FM spin structure of BaVSe$_3$ is not a simple [0,0,FM] but a canted [AF,0,FM]. Note that, in BaVS$_3$, the exchange interaction along the chain direction, i.e., the c axis, ($J_{ex}^c$) is known to be FM and very strong compared with the AF interchain (in plane) exchange interactions ($J_{ex}^{ab}$) [35]. Nevertheless, relatively weak $J_{ex}^{ab}$ plays
of V$^{4+}$ ions, which leads to the formation of CDW order [9,10,47]. As a result, the DM interaction is thought to be suppressed in BaVS$_3$, and the IC-AF ordered state is stabilized as a magnetic ground state [4,11].

Back to BaVSe$_3$, the $p$ dependence of $T_C$ clearly indicates the presence of two different exchange interactions in the $ab$ plane; i.e., one decreases $T_C$ with $p$, whereas the other increases $T_C$ with $p$. The former interaction is predominant up to around 1.5 GPa, while the latter overcomes the former at $p > 1.5$ GPa. The former interaction naturally corresponds to $J_{ex}^{ab}$ and the latter corresponds to the DM interaction. Since the interchain distance on the 2DTL decreases with increasing $p$, $J_{ex}^{ab}$ would be also enhanced with $p$. However, as $p$ further increases above 1.5 GPa, the noncentrosymmetric distortion is likely to be enhanced with $p$, leading to the increase in the DM interaction. On the contrary, $J_{ex}^{c}$ is also expected to be enhanced with $p$ through the decrease in the distance between the neighboring V ions in the chain, while such an enhancement is most unlikely essential for forming long-range magnetic order via the interchain interactions. To further elucidate the role of each interaction, we will need to study the crystal structure and magnetic anisotropy under $p$ using a single-crystal sample.

V. SUMMARY

We have investigated the microscopic magnetic nature of BaVSe$_3$ at ambient and high pressures with $\mu$+SR using a powder sample. The $\mu$+SR measurements in a ZF at ambient pressure clarified the appearance of a clear oscillatory signal below $T_C \sim 41$ K, which evidenced the formation of static FM order. Analyzing the internal magnetic field, it was suggested that the FM spin structure is not a simple one with an easy magnetization axis along the $c$ axis. The detailed analysis of the internal magnetic field suggested that the V moments align FM along the $c$ axis but slightly canted toward the $a$ axis by 28° that is coupled AF, namely, the ordered V moment ($M_V$) is $(0.59, 0, 1.11) \mu_B$.

The $\mu$+SR measurements in a wTF at high pressures showed that $T_C$ slightly decreases with pressure ($p$) up to 1.5 GPa, then $T_C$ increases rapidly with $p$ for $p > 1.5$ GPa. This suggested the presence of the two magnetic interactions in the $ab$ plane: one is an AF interaction, and the other is an FM interaction. The former is enhanced with $p$ up to 1.5 GPa, although the latter is predominant at $p > 1.5$ GPa.

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