Renal hemodynamics, function, and oxygenation during cardiac surgery performed on cardiopulmonary bypass: a modeling study

Ioannis Sgouralis1, Roger G. Evans2, Bruce S. Gardiner3, Julian A. Smith4, Brendan C. Fry1 & Anita T. Layton1

1 Department of Mathematics, Duke University, Durham, North Carolina
2 Department of Physiology, Monash University, Clayton, Victoria, Australia
3 Department of Computer Science and Software Engineering, University of Western Australia, Crawley, Western Australia, Australia
4 Department of Surgery, Monash University, Clayton, Victoria, Australia

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Abstract
Acute kidney injury, a prevalent complication of cardiac surgery performed on cardiopulmonary bypass (CPB), is thought to be driven partly by hypoxic damage in the renal medulla. To determine the causes of medullary hypoxia during CPB, we modeled its impact on renal hemodynamics and function, and thus oxygen delivery and consumption in the renal medulla. The model incorporates autoregulation of renal blood flow and glomerular filtration rate and the utilization of oxygen for tubular transport. The model predicts that renal medullary oxygen delivery and consumption are reduced by a similar magnitude during the hypothermic (down to 28°C) phase of CPB. Thus, the fractional extraction of oxygen in the medulla, an index of hypoxia, is increased only by 58% from baseline. However, during the rewarming phase (up to 37°C), oxygen consumption by the medullary thick ascending limb increases 2.3-fold but medullary oxygen delivery increases only by 33%. Consequently, the fractional extraction of oxygen in the medulla is increased 2.7-fold from baseline. Thus, the renal medulla is particularly susceptible to hypoxia during the rewarming phase of CPB. Furthermore, autoregulation of both renal blood flow and glomerular filtration rate is blunted during CPB by the combined effects of hemodilution and nonpulsatile blood flow. Thus, renal hypoxia can be markedly exacerbated if arterial pressure falls below its target level of 50 mmHg. Our findings suggest that tight control of arterial pressure, and thus renal oxygen delivery, may be critical in the prevention of acute kidney injury associated with cardiac surgery performed on CPB.

Introduction
Acute kidney injury (AKI) is a prevalent complication of cardiac surgical procedures that require cardiopulmonary bypass (CPB) (Karkouti et al. 2009). Even mild AKI following CPB cardiac surgery is prognostically important, being associated with a more than fourfold increase in the risk of in-hospital death (Karkouti et al. 2009) as well as extended hospital stays through additional complications (Karkouti et al. 2009). When AKI is severe enough to require renal replacement therapy (in 1–2% of patients who have undergone cardiac surgery under CPB), mortality rate exceeds 60% (Mangano et al. 1998).

Renal hypoxia might be an important pathway in the development of AKI during CPB cardiac surgery, particularly if there is a mismatch between changes in renal oxygen delivery and oxygen consumption (Evans et al. 2013). Renal oxygen delivery is mainly determined by renal blood flow (Evans et al. 2013). Renal oxygen consumption is mainly driven by the metabolic work of tubular sodium reabsorption, which in turn is largely driven by the filtered load of sodium, and thus glomerular filtration...
rate (GFR) (Evans et al. 2014). Mean arterial pressure is often set to a low level during CPB (50–70 mmHg), and further, autoregulation of renal blood flow and GFR is compromised (Andersson et al. 1994). Consequently, changes in renal blood flow and GFR during CPB will likely have a major impact on the risk of AKI.

Multiple factors compromise renal autoregulation during CPB. Firstly, the CPB circuit must be primed with a cell-free solution, resulting in hemodilution (Rosner et al. 2008). The potential importance of hemodilution is evidenced by the observation that a hematocrit of less than 21% is an independent risk factor for AKI after cardiac surgery (Rosner et al. 2008). Secondly, tissue perfusion during CPB is nonpulsatile. The pulsatility of renal arter- rial pressure is a critical determinant of the myogenic component of the autoregulatory response, as evidenced by experimental findings and simulations from mathematical models (Loutzenhiser et al. 2002; Chen et al. 2009; Sgouralis and Layton 2012). Collectively, these data indicate that oscillations in renal arterial pressure induced by the beating heart lead to sustained vasoconstriction of the afferent arteriole.

Thus, it seems reasonable to hypothesize that renal ischemia could arise during CPB as a result of complex interactions between the effects of altered blood viscosity due to hemodilution and hypothermia, the absence of pulsatility of blood flow, and hypotension. Clearly, our ability to study these phenomena in the clinical situation is limited. Our ability to study them in intact animals is also limited, because of the number of experimental conditions that would need to be met in order to allow such interactions to be fully interrogated. Therefore, in the current study we have utilized a computational model to examine how the renal hemodynamic changes during CPB might lead to renal circulatory dysfunction and hypoxia, and determine the phase during CPB in which the kidney is most vulnerable to hypoxic injury. Because anatomic data on the human kidney are limited, baseline model parameters are based on the rat, whose kidney is the most well studied, whereas clinical data from human patients are used to model the effects of CPB.

Mathematical Model

To model hemodynamic control and oxygenation in the kidney, we have extended a mathematical model, previously developed by us (Sgouralis and Layton 2014), which represents the functional unit of the kidney: a nephron with the supplying vessel. Specifically, the model consists of (1) an afferent arteriole; (2) a glomerulus; (3) a nephron. A schematic diagram of the model is shown on Figure 1. Briefly, the afferent arteriole delivers blood to the glomerulus. A portion of the plasma is filtered into the nephron, where fluid and sodium reabsorption takes place. The remaining blood is drained to the efferent arteriole and then distributed to either the cortex or medulla.

Autoregulatory mechanisms

Renal autoregulation is mainly mediated by the myogenic response and tubuloglomerular feedback, both of which regulate single nephron glomerular filtration rate (SNGFR) by inducing constriction or dilation of the afferent arteriole (Holstein-Rathlou and Marsh 1994; Cupples and Braam 2007; Just 2007). With the myogenic response, a rise in intravascular pressure elicits a reflex constriction that generates a compensatory increase in vascular resistance. Tubuloglomerular feedback is a negative feedback response that balances glomerular filtration with tubular reabsorptive capacity.

Renal blood flow

The afferent arteriole is the effector of the autoregulatory mechanisms. To properly simulate those mechanisms, the model afferent arteriole represents detailed ionic transport and muscle mechanics of a series of arteriolar smooth muscle cells, coupled electrically. Each arteriolar smooth muscle cell incorporates cell membrane potential, transmembrane ionic transport, cytosolic Ca2+ regulation, and muscle contraction. Key model equations can be found in the Appendix 1. Vascular flow is described as quasi-steady Poiseuille flow. Thus, given renal perfusion pressure (RPP), the arteriolar model predicts blood flow QAA.

Glomerular filtration

The model glomerulus is represented as a single capillary, connected between the afferent and efferent arterioles. Model equations are based on conservation of plasma and protein. Plasma filtration is characterized by the ultrafiltration coefficient Kt (see Appendix 1). Given arteriolar outflow QAA, the glomerulus model predicts SNGFR. We assume that 90% of the efferent arteriolar flow is directed to the cortex, and the remaining 10%, denoted fmed, to the medulla. Thus, the flow of red blood cells to the medulla is given by

\[
Q_{RBC}^{med} = f_{med} H_{med} (Q_{AA} - SNGFR), \tag{1}
\]

where \(H_{med}^{med}\) denotes the medullary hematocrit, which is 20% lower than systemic hematocrit (Zimmerhackl et al. 1985). Plasma flow is given by

\[
Q_{plasma}^{med} = \frac{1 - H_{med}^{med}}{H_{med}^{med}} Q_{RBC}^{med}
\]
Oxygen delivery to the medulla (denoted $D_{med}$) is given by the total amount of free and hemoglobin-bound oxygen (Popel 1989)

$$D_{med}^{O_2} = \left[ O_2 \right]_{free}^\text{plasma} + \left[ HbO_2 \right]_RBC^\text{plasma}$$

(Tubular transport)

The model nephron comprises a proximal tubule and a short loop of Henle. The model predicts intratubular pressure, water flow, and tubular fluid $[Cl^-]$, which is the key signal to tubuloglomerular feedback (see below). Tubular fluid $[Cl^-]$ is given by conservation of mass

$$\frac{\partial}{\partial t} \left( \pi R_{neph,ss}^2 [Cl^-] \right) = -\frac{\partial}{\partial x} \left( Q_{neph} [Cl^-] \right) - J_{act} - J_{pass}$$

where $R_{neph}$ is tubular luminal radius, which is assumed to vary passively with luminal fluid pressure, and $Q_{neph}$ is the tubular fluid flow. $J_{act}$ and $J_{pass}$ denote the active and passive transport of $Cl^-$, respectively, assumed positive into the tubule

$$J_{act} = 2\pi R_{neph,ss} \frac{V_{max} [Cl^-]}{K_M + [Cl^-]}$$

$$J_{pass} = 2\pi R_{neph,ss} p_{neph} ([Cl^-]_{int} - [Cl^-])$$

$R_{neph,ss}$ denotes the steady-state radius. Active transport is assumed to be characterized by Michaelis–Menten kinetics, which is an approximation for the membrane transport processes that include the cotransport of $Na^+$, $K^+$, and (two) $Cl^-$ ions by the apical NKCC2 transporter, the active transport by $Na^+$ ion via the basolateral $Na^+/K^+$-ATP pump, and the passive diffusion of the $Cl^-$ ion through the basolateral membrane. Passive transepithelial diffusion is characterized by permeability $p_{neph}$. Interstitial $[Cl^-]$, denoted $[Cl^-]_{int}$ is assumed known a priori.

Based on $Na^+/K^+$-ATPase stoichiometry, which suggests that at maximum efficiency, 18 moles of $Na^+$ are transported per mole of $O_2$ consumed, we compute the rate of $O_2$ consumption due to active transport by $J_{act}/18$. Thus, total $O_2$ consumption by the medullary structures, given

Figure 1. Schematic representation of the renal model. Blood is supplied through the afferent arteriole. In the glomerulus, a portion of the delivered plasma is directed to the proximal tubule, and the rest to the efferent arteriole. Cortical and medullary capillary beds are supplied by the efferent arteriole outflow. The afferent arteriole is shown with five smooth muscles (SM), whereas in the model 101 SM are represented.
per nephron, is determined by summing the total O$_2$ consumption rate by the medullary segments (i.e., proximal straight tubule and, most importantly, the medullary thick ascending limb) and the basal consumption, that is,

$$V_{\text{total}} = \int \frac{\text{act}}{18} \, dx + V_{\text{basal}}.$$  \hspace{1cm} (6)

The integral is computed over the medullary segments only. $V_{\text{basal}}$ denotes basal consumption per nephron, that is, total basal O$_2$ consumption in the medulla, divided by the number of nephrons. Medullary basal O$_2$ consumption is set to 0.70 pmol/min/nephron, based on (Fry et al. 2014).

### Results

#### Impact of hypothermia

We first studied the effects of temperature on renal function by simulating two non-CPB scenarios, normothermia (base case), and hypothermia, in which body temperature is assumed to be 37°C and 28°C, respectively. Key model parameters for these cases are summarized in Table 1. A comparison between renal function predicted in the normothermic and hypothermic cases indicate the substantial effect of hypothermia on blood flow and oxygenation (Table 2). A comparison between model predictions and experimental findings reported in (Broman and Källskog 1995) validates the model.

The model represents the following temperature-dependent phenomena. For simplicity, model parameters are fitted as linear functions to the available data at 37°C and 28°C.

1. We assume that *afferent arteriole myocyte cytosolic [Ca$^{2+}$]* increases at lower temperature. This is achieved by decreasing afferent arteriole smooth muscle cytosolic Ca$^{2+}$ extrusion rate with temperature (Broman and Källskog 1995).

2. We assume that *efferent arteriole muscle activation* increases with temperature (Broman and Källskog 1995).

3. *Plasma and tubular fluid viscosities* increase with decreasing temperature (Broman and Källskog 1995; Lim et al. 2010).

4. The *ultrafiltration coefficient* $K_f$ decreases with decreasing temperature (Broman and Källskog 1995).

5. Broman and Källskog (Broman and Källskog 1995) reported GFR, urine flow and composition produced by groups of rats with body temperate kept at 37°C and 28°C, respectively, and whose kidneys were moderately concentrating. Based on these data, we assume that *thick ascending limb maximum transport rate* $V_{\text{max}}$ decreases with decreasing temperature. Model formula-

| Table 1. Parameter values for the simulated cases. The normothermic and hypothermic cases are motivated by (Broman and Källskog 1995), and the CPB phases are motivated by (Andersson et al. 1994). |
|-----------------|-----------------|-----------------|-----------------|-----------------|-----------------|-----------------|-----------------|
| Renal perfusion pressure | 120 mmHg | 120 mmHg | 75 mmHg | 50 mmHg | 50 mmHg | 75 mmHg | Units |
| Pulse amplitude | 20 mmHg | 20 mmHg | 20 mmHg | 0 mmHg | 0 mmHg | 20 mmHg |
| Systemic hematocrit | 45 % | 45 % | 45 % | 25 % | 25 % | 25 % |
| Body temperature | 37 °C | 28 °C | 37 °C | 28 °C | 37 °C | 37 °C |
| Arterial PO$_2$ | 100 mmHg | 100 mmHg | 100 mmHg | 400 mmHg | 400 mmHg | 100 mmHg | Units |

| Table 2. Comparison of simulated normo- and hypothermia. Renal blood flow, Henle’s loop flow, nL/min/nephron; SNGFR, nL/min; glomerular blood pressure (BP), Bowman space pressure, mmHg; net NaCl reabsorption, pmol/min/nephron. |
|-----------------|-----------------|-----------------|-----------------|-----------------|-----------------|-----------------|
| Renal blood flow | 290.3 nL/min | 156.6 nL/min | Model | Ref. (Broman and Källskog 1995) |
| SNGFR | 30.0 nL/min | 15.8 nL/min | −46.1 % | −44.5 % |
| Glomerular BP | 50.7 mmHg | 45.0 mmHg | −11.3 % | −18.2 % |
| Bowman pressure | 14.0 mmHg | 13.9 mmHg | −0.5 % | −2.5 % |
| Henle’s loop flow | 8.8 nL/min | 4.6 nL/min | −48.4 % | −49.3 % |
| Net reabs. | 3048 pmol/min | 1577 pmol/min | −48.3 % | −49.3 % |
tion (Appendix 1 Eq. (A36)) assumes zero time lag between the increase in temperature and the adjustment of active tubular transport.

In large part owing to the slower Ca\(^{2+}\) extrusion rate at low temperatures, smooth muscle cytosolic [Ca\(^{2+}\)] increases with decreasing temperature; see Figure 2A. The elevated cytosolic [Ca\(^{2+}\)] leads to vasoconstriction and reduction in blood flow and SNGFR; Figure 2B. The observed temperature mediated reduction in blood flow and SNGFR is further amplified by the rise in blood viscosity and decrease in glomerular filtration coefficient.

At 28°C, the model predicts a marked 46.1% decrease in arteriolar flow, which results in a 47.4% reduction in SNGFR. In addition to its effect on blood flow, lower temperature also reduces thick ascending limb active transport. As a result, the model predicts a 48.3% lower NaCl reabsorption rate in the hypothermic case. This yields an elevated luminal [Cl\(^-\)] at the macula densa (53.0 vs. 46.1 mmol/L), which activates tubuloglomerular feedback and further reduces SNGFR. The relative changes reported above are in good agreement with the measurements of Broman and Källskog (Broman and Källskog 1995) (Table 2).

Renal function and hemodynamics during CPB

In the next set of simulations, we aimed to identify the phase in CPB when the kidney is most vulnerable to hypoxic injury. Four CPB phases were considered: (1) pre-CPB, defined as the period following induction of anesthesia and prior to initiation of CPB; (2) hypothermic CPB, the hypothermic period of the surgery; (3) CPB rewarming, the normothermic period of the surgery; and (4) post-CPB, the post-surgery period in which the effects of hemodilution and anesthesia persist. Model parameters for these cases are given in Table 1.

Besides body temperature (lower in hypothermic CPB), hemodynamics also differ substantially among the four CPB phases.

1 Notably, due to the effects of anesthesia, RPP is lower than baseline in all four phases, but particularly so during the hypothermic CPB and CPB rewarming phases.

2 During the pre- and post-CPB phases, blood circulation is driven by the heart. The resulting pulsatile flow is modeled by

\[
RPP = 75 \text{ mmHg} + 20 \text{ mmHg} \times \sin(2\pi f t),
\]

where the frequency \(f\) is set to 1 Hz and \(t\) is given in seconds. The CPB pump used during surgery does not generate pulsatile flow. Thus, RPP is assumed constant at 50 mmHg for the hypothermic CPB and CPB rewarming phases.

3 Except for the pre-CPB phase, systemic hematocrit is substantially lower than normal. A lower hematocrit results in a lower effective blood viscosity (Pries et al. 1992; Pries and Secomb 2003), which the model accounts for by incorporating the empirical hematocrit–viscosity relation obtained by Pries et al. in (Pries et al. 1994) (equation (9) therein).

4 The impact of hemodilution on oxygen delivery is partially compensated by the ventilation of the patient with almost 100% oxygen during the hypothermic CPB and CPB rewarming phases.

Key renal function and hemodynamic predictions are summarized in Table 3 and Figure 3. The pre-CPB phase differs from baseline only in a lower RPP (75 vs. 100 mmHg). The lower RPP triggers a myogenic response that induces vasodilation which stabilizes renal blood flow and SNGFR. The effectiveness of the model myogenic response can be seen in Figure 4, which shows predicted time-averaged blood flow for a range of mean arterial pressures, obtained for pulsatile and steady RPP. The model predicts efficient autoregulation between 80 and 115 mmHg when RPP is pulsatile, which is somewhat blunted when RPP is nonpulsatile. Given a RPP of
75 mmHg during the pre-CPB phase, the model predicts 13.4% and 6% reductions in blood flow and SNGFR.

Hemodilution begins during the hypothermic phase of CPB. Taken in isolation, the lower blood viscosity at a lower hematocrit would increase blood flow. However, RPP is further reduced to 50 mmHg, which, as seen in Figure 4, falls below the range of RPP where autoregulation can sufficiently compensate for the pressure variations and stabilize SNGFR. Furthermore, temperature is decreased to 28°C. As shown in the preceding set of simulations, hypothermia markedly decreases blood flow and SNGFR. Together, these factors result in a 53.8% reduction in arteriolar blood flow, and a 61.3% reduction in SNGFR. The drastically lowered medullary blood flow (MBF) and hemodilution decrease medullary oxygen delivery, which is only partially compensated for by the fourfold increase in blood PO2. Consequently, medullary oxygen delivery is only 29.4% that of the base case, its minimum level of all the phases of CPB.

With the transition to the rewarming phase of CPB, body temperature is restored to 37°C, resulting in substantially greater renal blood flow and SNGFR compared to the hypothermic phase, although those flows remain substantially lower than in the base case. (Body temperature likely increases gradually from 28°C to 37°C; however, here we consider only the final body temperature of 37°C.) A particularly notable effect of a higher body temperature is the increase in thick ascending limb active transport. Consequently, medullary O2 consumption is 129% greater than in the hypothermic phase of CPB.

| Renal blood flow | Base case | Pre-CPB | CPB-hypothermia | CPB-rewarming | Post-CPB |
|------------------|-----------|---------|-----------------|---------------|----------|
| SNGFR            | 290.3     | 251.2   | 134.2           | 180.9         | 420.3    |
| Filtration %     | 30.0      | 28.2    | 11.6            | 17.2          | 30.9     |
| Active reabs.    | 283.1     | 294.4   | 123.7           | 299.7         | 292.3    |
| O2 delivery      | 168.2     | 168.2   | 57.1            | 75.7          | 158.8    |
| O2 consumption   | 10.1      | 10.1    | 13.3            | 22.9          | 10.7     |
| Consumption %    | 8.4       | 10.1    | 13.3            | 22.9          | 10.7     |

*Table 3. Summary of renal function during CPB. Renal blood flow, nL/min/nephron; SNGFR, nL/min; medullary active NaCl reabsorption, O2 delivery, O2 consumption, pmol/min/nephron.*
Thus, even though medullary oxygen delivery is greater in the rewarming phase of CPB than the hypothermic phase, the rewarming phase is associated with a greater medullary fractional O₂ extraction (22.9%, compared to 13.3% in the hypothermic phase of CPB and 8.4% in the base case).

The predicted PO₂ at different CPB phases exhibit trends that are consistent with a pilot study in pigs (Stafford-Smith and Grocott 2005).

**Impact of variations in surgical conditions**

During each phase of the CPB surgery, hematocrit likely fluctuates substantially. To determine the effects on renal oxygenation, we simulated the CPB hypothermic and rewarming phases for a range of hematocrit values, and computed the resulting O₂ fractional extraction. Simulation results, shown in Figure 5, indicate that large declines in hematocrit yield substantial increases of O₂ consumption, with the effect being significantly more prominent during the rewarming phase.

The interstitial [NaCl] axial gradient along the outer medulla is generated primarily by the metabolically driven Na⁺ reabsorption from the thick ascending limb. At low temperatures, Na⁺ reabsorption is slowed, which may lower the interstitial [NaCl]. To assess the model’s response to changes in interstitial [NaCl], we simulated the CPB hypothermic and rewarming phases with interstitial [Cl⁻] reduced by 50%. That is, interstitial [Cl⁻] increases from 115 mmol/L at the corticomedullary boundary to 195 mmol/L (compared to 275 mmol/L in the base case) at the outer-inner medullary boundary. Key predictions, shown on Table 4, suggest that model results are mostly insensitive to changes in interstitial [NaCl], owing, in large part, to the small permeability of the thick ascending limbs (1.5 × 10⁻⁵ cm/sec).

Having identified rewarming as the CPB phase with the largest fractional medullary O₂ consumption, and thus the highest degree of vulnerability to renal hypoxic injury, we consider the effects on renal function of varying RPP, hematocrit, and the degree of MBF autoregulation during rewarming. In volume-expanded rats, MBF has been observed to be autoregulated to a lesser extent than renal blood flow (Fenoy and Roman 1991; Mattson et al. 1993). To incorporate that finding, we modify Equation 3.
tion (1) as follows

$$Q_{\text{RBC}}^{\text{med}} = H_{\text{med}}^{\text{med}} (Q_{AA} - \text{SNGFR}) + b \frac{\text{MBF}}{\text{RPP}} (\text{RPP} - \text{RPP}^*)$$

where $b$ controls the degree of MBF autoregulation and the asterisks denote reference values. In the base case, $b$ is set to 0 (best autoregulation).

We conducted simulations in which the CPB rewarming was used as the reference phase. In particular, reference RPP is 50 mmHg, hematocrit 25%, and body temperature 37°C. In three sets of simulations, we computed fractional medullary O2 consumption for a range of values of RPP and hematocrit. For each set of simulations, we also varied the degree of MBF autoregulation by setting $b = 0, 10\%, 20\%, \text{and} 30\%$. Results are shown in Figure 6. The model predicts that a reduction in RPP has the most marked effect on medullary oxygenation. As previously noted, RPP during surgery on CPB often falls below the range of values that autoregulation can adequately compensate for (Brady et al. 2010). Thus, the model predicts that, with the most robust autoregulation of MBF, decreasing RPP to 30 mmHg (Brady et al. 2010), a value that is by no means atypical during surgery on CPB, decreases SNGFR, decreases medullary O2 delivery, and dramatically raises medullary O2 consumption to nearly 100% of O2 delivery. When MBF autoregulation is less robust (for example $b = 30\%$), a similarly high fractional oxygen extraction can be obtained at RPP as high as ~45 mmHg.

**Impact of variations in temperature during the hypothermic phase of cardiopulmonary bypass**

Our model assumes a temperature of 28°C in the hypothermic phase of cardiopulmonary bypass. However, routine procedures for cardiac surgical patients may be performed at higher temperatures of 32–34°C, whereas major aortic cases are often cooled to 18°C. Thus, we study the impact of variations in temperature during the hypothermic phase on medullary fractional oxygen extraction. Results are shown in Figure 7. The dependence of oxygen extraction fraction on temperature is nonmonotonic owing to the competing effects of higher tubular active NaCl reabsorption rate and increased medullary blood flow (thus O2 supply) as temperature increases. The fractional extraction of oxygen markedly increases as temperature is raised from 28°C (13%) to 34°C (20%), thereby rendering the medulla at a much higher risk to hypoxic injury. For comparison, the fractional extraction of oxygen was calculated to be 23% at 37°C.

**Discussion**

The principal goal of this study was to determine the phase or phases of cardiac surgery on CPB during which the renal medulla is most susceptible to hypoxia, and the renal hemodynamic and functional factors that drive this

![Figure 6. Renal oxygenation sensitivity during CPB rewarming. Medullary O2 fractional consumption as a function of renal perfusion pressure (A), hematocrit (B), and body temperature (C). For all simulations, arterial blood PO2 is 400 mmHg and RPP is nonpulsatile. Reference state is at RPP of 50 mmHg, hematocrit of 25%, and body temperature 37°C (denoted by dotted lines). The four curves in each of the panel correspond to differing degrees of MBF autoregulation (b).](image)

![Figure 7. Fractional extraction of O2 in the medulla during the hypothermic phase of CPB, as a function of body temperature.](image)
susceptibility. Simulation results have identified the rewarming phase of CPB, in which medullary blood flow is low but medullary oxygen consumption remains high, as the phase in which the kidney is the most vulnerable to hypoxic injury (Fig. 3). The model predicts that during the rewarming phase of CPB, 22.9% of the medullary O2 supply is consumed. Since net medullary O2 supply exceeds consumption by a comfortable margin, it may not be immediately clear how such an effect might render the medulla susceptible to hypoxic damage. The explanation lies in the anatomy of the kidney: the spatial arrangement of nephrons and vessels has been found to be highly structured in a number of mammalian kidneys (Kriz 1981), including rats, mice, and human (Kriz 1967; Kriz et al. 1972; Kriz and Koepsell 1974; Jamison and Kriz 1982). The structural organization of the renal vasculature limits oxygen delivery to renal tissue, as discussed below.

In the outer medulla, vasa recta form tightly packed vascular bundles that appear to dominate the histotopography, especially in the inner stripe. Collecting ducts and thick ascending limbs are found distant from the bundles. The sequestration and countercurrent arrangement of the descending and ascending vasa recta preserves O2 delivery to the inner medulla (Chen et al. 2009). However, given the high metabolic demand of the thick ascending limbs, their separation from the oxygen-carrying descending vasa recta subjects the thick limbs to risk of hypoxia. PO2 in the inner medulla is lower than in the outer medulla (Evans et al. 2013), but the thin ascending limbs in the inner medulla do not mediate significant active NaCl transport and thus have much lower oxygen demand. Thus, we focus our discussion on the outer medulla.

Measurements of PO2 in the renal outer medulla typically range from 20 to 30 mmHg (Dinour and Brezis 1991; Brezis et al. 1994; Liss et al. 1998; dos Santos et al. 2007; Palm et al. 2008). However, the structural organization of the tubules and vessels likely results in a substantial radial gradient in PO2. A recent study (Fry et al. 2014) using a detailed mathematical model of O2 transport in the renal medulla indeed predicts such a radial gradient in interstitial PO2, from as high as ~35 mmHg in the core of the vascular bundle, to as low as ~5 mmHg in the interbundle region. The model thick ascending limbs operate near anoxia, with average luminal PO2 as low as 2.5 mmHg in the inner stripe.

The results we present were computed using baseline model parameters, which implicitly assume conditions similar to the case of normothermia in the present study. When vascular inflow and hematocrit were lowered to simulate conditions in the rewarming phase of CPB, thereby lowering O2 supply, thick limb luminal PO2 fell to 1.25 mmHg (Fry et al. 2014). Simulations using the present model indicate that the risk of hypoxia can markedly increase even with a modest decrease in RPP during surgery (Fig. 6A). This result has a troubling implication, because of the technical difficulties in stabilizing perfusion pressure within a narrow range during CPB. In fact, during surgery perfusion pressure can fall to as low as 30 mmHg (Brady et al. 2010), which exposes the patients to serious risk of renal hypoxia. This pathway to hypoxic injuries is summarized in Figure 8.

The present model assumes the MBF is approximately a constant fraction of renal blood flow. However, measurements by Mattson et al. (Mattson et al. 1993) indicate that cortical blood flow is significantly better autoregulated than MBF as RPP varies. This implies that our model may overestimate MBF at low perfusion pressure, and underestimate the extent of medullary hypoxia.

A key mechanism by which CPB affects renal hemodynamics and oxygenation is through the effects of hypothermia, which include vascular tone, plasma viscosity, glomerular filtration, and metabolism. However, relevant data are sparse. Thus, to model kidney function during CPB, we have made assumptions based almost entirely on a single study, that by Broman and Källskog (Broman and Källskog 1995). Without supporting measurements from additional studies, it is unclear how robust those assumptions are. It is noteworthy that the model’s key prediction, that the kidney is particularly vulnerable to hypoxic injury during the rewarming phase (as opposed to the hypothermic phase), depends rather critically on the kidney’s metabolic demand, which is attributable in no small part to the active transport of the renal tubules. However, how tubular active transport varies as a func-

![Figure 8. Pathway for the development of hypoxic injury.](image)
tion of body temperature has not been quantified, and we have made model assumptions based on urine flow and composition measured by Broman and Källskog (Broman and Källskog 1995) in hypothermic and normothermic rats. Given the critical role of metabolism in renal oxygen demand, more precise measurements would strengthen the model’s prediction and yield a better understanding of the risk of AKI during different CPB phases.

**Conflict of Interest**

None declared.

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Appendix: Model Equations

The present model is an extension of a mathematical model of renal hemodynamic control previously developed by us (Sgouralis and Layton 2014). A schematic representation is shown on Figure 1. The model consists of a large set of equations and parameters, which can be found in (Sgouralis and Layton 2014) and the references therein. Below we summarize some of the key model equations, and highlight the modifications made to include the effects temperature and hemodilution that are not captured in (Sgouralis and Layton 2014).

Autoregulatory mechanisms

The afferent arteriole is the effector site of the myogenic mechanism and tubuloglomerular feedback (TGF). The model afferent arteriole segment consists of a series of smooth muscle cell models. Each smooth muscle model incorporates membrane potential, transmembrane ionic transports, cytosolic Ca2+ regulation, and muscle contraction. The rate of change in the membrane potential \( V_m \) of the i-th smooth muscle is given by the sum of transmembrane currents

\[
\frac{dV_m^i}{dt} = -I_{M}^{i}(t) - I_{K}^{i}(t) - I_{Ca}^{i}(t) + I_{m-m}^{i}(t) + I_{m-e}^{i}(t)
\]

(A1)

where \( C_m \) denotes the cell capacitance, and \( I_{M}, I_{K}, I_{Ca} \), \( I_{m-m}, I_{m-e} \) denote transmembrane leak current, potassium current, calcium current, gap junctional current between smooth muscles, and gap junctional current between smooth muscle and the endothelium, respectively. The remaining currents, \( I_{MB}^{i} \) and \( I_{TGF}^{i} \), arise from the operation of the myogenic response and TGF, described below.

With the myogenic response, a rise in intravascular pressure elicits a reflex constriction that generates a compensatory increase in vascular resistance, after an initial delay of \( \tau_m \). The overall response time is faster for vasodilation than vasodilation (Loutzenhiser et al. 2002, 2004). To capture this response, the model assumes that the activity of nonselective cation channels is shifted by changes in intravascular pressure, such that the smooth muscle membrane depolarizes with increasing intravascular pressure and vice versa. This process is represented by
the pressure-dependent current $I^\text{MR}_{\text{MR}}$ in Equation (A1) given by
\[
\frac{dI^\text{MR}_{\text{MR}}}{dt} = -k_{\text{MR}} \times (I^\text{MR}_{\text{MR}}(t) - I^\text{MR}_{\text{MR}}(P^\text{PA}_{\text{AA}}(t - \tau_\text{m}) - P^\text{T}_{\text{AA}})).
\]
(A2)

where $P^\text{PA}_{\text{AA}}$ denotes the intravascular pressure. The rate constant $k_{\text{MR}}$ at time $t$ depends on the direction in which $P^\text{PA}_{\text{AA}}$ is changing at an earlier time $t - \tau_\text{m}$. The target myogenic current $I^\text{MR}$ is assumed to be a sigmoidal function of the deviation of $P^\text{PA}_{\text{AA}}$ from its baseline value $P^\text{T}_{\text{AA}}$.

The TGF signal is represented by the current $I^\text{TGF}_i$ which is applied to the smooth muscles spanning the distal 60 µm of the afferent arteriole. The current $I^\text{TGF}_i$ is assumed to exhibit a sigmoidal dependence on the deviation of the intratubular macula densa [Cl] from its operating point.

The myogenic response and TGF affect membrane potential $v^\text{mem}$, which in turns changes the opening probability of the voltage-gated Ca$^{2+}$ channels and the associated flux $I^\text{Ca}_i$. Smooth muscle-free cytosolic Ca$^{2+}$ concentration, denoted $c^\text{i}$ (in nmol/L), is assumed in equilibrium with the buffer and is related to $I^\text{Ca}_i$ (given in mV/sec) by
\[
\frac{dc^\text{i}}{dt} = \frac{(10^3 + c^\text{i}(t))^2}{(10^3 + c^\text{i}(t))^2 + 10^9} \times (-628 \times I^\text{Ca}_i(t) - k_{\text{Ca}}c^\text{i}(t)),
\]
(A3)

where $k_{\text{Ca}}$ is the first-order rate constant for cytosolic calcium extrusion (Chen et al. 2011). We assume that afferent arteriole myocyte cytosolic [Ca$^{2+}$] increases at lower temperature. This is achieved by decreasing afferent arteriole smooth muscle cytosolic Ca$^{2+}$ extrusion rate with temperature (Broman and Källskog 1995) by assuming the following dependence on temperature
\[
k_{\text{Ca}} = 190 + 4.27 \times (T - 37.0).
\]
(A4)

Temperature effects, here and below, are modeled by linear curves fitted to the available data at 37°C (reference temperature) and 28°C (Broman and Källskog 1995). Cytosolic [Ca$^{2+}$] determines the phosphorylation level $\psi^\text{i}$
\[
\psi^\text{i}(t) = \frac{(c^\text{i}(t))^{3/2}}{400^3 + (c^\text{i}(t))^{3/2}},
\]
(A5)

which, in turn, determines the fraction of formed cross-bridges, denoted $\omega^\text{i}$, according to
\[
\frac{d\omega^\text{i}}{dt} = 0.318 \times \left(\frac{\psi^\text{i}(t)}{\psi^\text{i}(t) + 0.55} - \omega^\text{i}(t)\right),
\]
(A6)

where $\omega^\text{i}$ determines the active wall tension of the smooth muscle cells, and thus the luminal radius of the afferent arteriole.

Efferent arteriole luminal radius is determined similarly, with the exception that the crossbridge formation value, $\omega^\text{EA}$, depends on temperature but not pressure, inasmuch as the efferent arteriole is myogenically inactive. We assume that efferent arteriole muscle activation increases with temperature (Broman and Källskog 1995); thus, we have
\[
\omega^\text{EA} = 0.100 - 0.00136 \times (T - 37.0).
\]
(A7)

Renal blood flow

To compute vascular blood flow, we assume that the model afferent arteriole is connected in series to a pre-afferent arteriolar resistor $\Omega^\text{RA}$ and a post-afferent arteriolar resistor $\Omega^\text{EA}$. The pre-afferent arteriolar resistance (in mmHg-sec/nL) is assumed to be a function of hematocrit, given by
\[
\Omega^\text{RA} = \frac{\mu^\text{plasma}}{\pi} \left(0.0112 \left(1 - \frac{H_t^\text{plasma}}{0.762}\right)\right).
\]
(A8)

The overall resistance of the model afferent arteriole is computed from the radius profile
\[
\Omega^\text{EA}(t) = \frac{8\mu^\text{AA}}{\pi} \int_0^{L^\text{AA}} \frac{dz}{R_{\text{AA}}^4(t, z)}
\]
(A9)

where $L^\text{AA} = 303 \mu$m is afferent arteriole length, and $\mu^\text{AA}$ denotes blood viscosity, which is a function of hematocrit
\[
\mu^\text{AA} = \frac{7.55}{(1 - H_t^\text{plasma})^{0.26}} - 0.00768.
\]
(A10)

The representation of the impact of hemodilution on blood viscosity follows the approach of Pries et al. (Pries et al. 1992) (equation 9 therein). The component $\mu^\text{plasma}$ (in mPa-sec) is a function of temperature (Lim et al. 2010), given by
\[
\mu^\text{plasma} = 1.70 - 0.0472 \times (T - 37.0).
\]
(A11)

Postglomerular resistance is computed by
\[
\Omega^\text{EA}(t) = \frac{8\mu^\text{EA}(t)}{\pi} \frac{L^\text{EA}}{R_{\text{EA}}^4(t)},
\]
(A12)

where $L^\text{EA}=303 \mu$m denotes the efferent arteriole length, and $\mu^\text{EA}$ is the postglomerular viscosity, given by
\[
\mu^\text{EA}(t) = \frac{7.71}{(1 - H_t^\text{plasma}(t)^{0.26}) - 4.26}.
\]
(A13)

The evaluation of postglomerular hematocrit $H_t^\text{EA}$ accounts for plasma loss due to filtration and is given by
below). Pressure at the end of the postglomerular segment to the estimated transit time along the glomerular bed. Thus, cardiac oscillations are expected to be significantly damped by the process of glomerular filtration. To account for such damping, \(Q_{AA}(t)\) and \(P_{\text{out}}^{AA}(t)\) are passed through a linear low pass filter

\[
\begin{align*}
\frac{dQ_{\text{AA}}^s}{dt} &= \frac{1}{\tau_{GL}} \left( Q_{\text{AA}}(t) - Q_{\text{AA}}^s(t) \right), \\
\frac{dP_{\text{out}}^{\text{AA}}}{dt} &= \frac{1}{\tau_{GL}} \left( P_{\text{out}}^{\text{AA}}(t) - P_{\text{out}}^{\text{AA}}^s(t) \right),
\end{align*}
\]

where the time constant \(\tau_{GL} = 0.61\) s is chosen according to the estimated transit time along the glomerular bed.

Let \(Q_{GL}\) and \(C_{GL}\) denote the plasma flow and plasma protein concentration profiles, respectively. Based on conservation of plasma mass, we have

\[
\frac{\partial Q_{GL}}{\partial y} = -K_f \times \left( P_{GL}(t,y) - P_{\text{neph}}(t,0) - \pi(t,y) \right),
\]

where \(y\) denotes position along the glomerular capillary, \(P_{\text{neph}}(t,0)\) denotes the proximal tubule inflow pressure and \(\pi\) denotes the colloid osmotic pressure (a function of \(C_{GL}\); see Sgouralis and Layton 2014). \(K_f\) (in \(\text{nl/min/mmHg}\)) is the ultrafiltration coefficient, assumed to exhibit the following temperature dependence

\[
K_f = 2.14 + 0.0119 \times (T - 37.0).
\]

\(P_{GL}\) is the hydrostatic blood pressure, assumed to decrease linearly along the capillary

\[
P_{GL}(t) = P_{\text{out}}^{\text{AA}}(t) - y \frac{\Delta P_{GL}}{L_{GL}}.
\]

where \(\Delta P_{GL}\) (in mmHg) is the total pressure drop (i.e., \(P_{GL}(t,0) - P_{GL}(t,L_{GL})\)), and is assumed to depend on hematocrit

\[
\Delta P_{GL} = \mu_{\text{plasma}} \times \left( \frac{1.55}{1 - Ht}^{1.07} - 1.17 \right).
\]

Plasma enters the glomerular capillary at a rate determined by hematocrit and arteriolar blood flow

\[
Q_{GL}(t,0) = (1 - Ht) \times Q_{AA}^s(t).
\]

SNGFR is given by the total fluid flux along the capillary

\[
\text{SNGFR}(t) = Q_{GL}(t,0) - Q_{GL}(t, L_{GL}).
\]

Oxygen delivery to the medulla is given by the total amount of free and bound oxygen (see Eq. (2) in main text).

Free and bound oxygen concentrations are given by the standard formulas (Popel 1989)

\[
[O_2]_{\text{free}} = \sigma_{\text{plasma}} \cdot PO_2, \quad [\text{HbO}_2] = 4c_{\text{Hb}} S_{\text{Hb}},
\]

where \(\sigma_{\text{plasma}}\) (in \(\text{nmol/L/mmHg}\)) is oxygen solubility in plasma, which depends on temperature (Christoforides and Hedley-Whyte 1969; Christoforides et al. 1969). Following the approach in Ref. (Battino et al. 1983), we assume that

\[
\sigma_{\text{plasma}} = 1.34 \times \exp \left( \frac{37.0 - T}{53.7} \right).
\]

In the expression for \([\text{HbO}_2]\) in Eq. (A25), \(c_{\text{Hb}} = 4.75\) mmol/L is concentration of hemoglobin in erythrocytes, and \(s_{\text{Hb}}\) is the saturation modeled by the Hill equation

\[
s_{\text{Hb}} = \frac{PO_2^{50}}{PO_2^{50} + PO_2^{2.50}}.
\]

The temperature dependence of \(P_{50}\) (in mmHg) is estimated experimentally in (Samaja et al. 1983) to be

\[
P_{50} = 26.0 \times \exp \left( -9.11 - \frac{2150}{T - 273} \right).
\]

**Tubular transport**

The model renal tubule includes a proximal tubule and a short loop of Henle. The model predicts intratubular
pressure $P_{\text{neph}}$, water flow $Q_{\text{neph}}$, and $[\text{Cl}^-]$ profiles. Tubular water flow is pressure driven

$$\frac{\partial P_{\text{neph}}}{\partial x} = -\frac{8 \mu_{\text{neph}}}{\pi R_{\text{neph}}^4(t,x)} Q_{\text{neph}}(t,x), \quad (A29)$$

where the temperature dependence of tubular fluid viscosity (in dyn/sec/m²) is given by

$$\mu_{\text{neph}} = 72.0 - 7.23 \times (T - 37.0), \quad (A30)$$

The proximal tubule and the initial segment of the descending limb of Henle's loop are water permeable. Taking the transmural water flux $\Phi_{\text{neph}}$ into account, pressure and flow are given by

$$\frac{\partial Q_{\text{neph}}}{\partial x} = -2\pi R_{\text{neph}}(t,x) \frac{\partial R_{\text{neph}}(t,x)}{\partial t} - \Phi_{\text{neph}}(t,x), \quad (A31)$$

Water flow entering the proximal tubule equals SNGFR. Transmural water flux is determined by SNGFR and renal perfusion pressure (RPP)

$$\Phi_{\text{neph}}(t,x) = S_{\text{GTB}}(\text{SNGFR}) \times S_{\text{PN}}(\text{RPP}) \times \Phi_{\text{neph}}^{\text{base}}(x), \quad (A32)$$

where RPP denotes time-averaged RPP, and $\Phi_{\text{neph}}^{\text{base}}$ is the baseline water flux profile, see Ref. (Sgouralis and Layton 2014). The factor $S_{\text{GTB}}(\text{SNGFR})$ models glomerulotubular balance (Thomson and Blantz 2008; Thomson et al. Jan 2001)

$$S_{\text{GTB}}(\text{SNGFR}) = \frac{1}{1 + \kappa_{\text{GTB}} \times \left( \frac{30.0}{\text{SNGFR}} - 1 \right)}, \quad (A33)$$

where SNGFR is given in nL/min. Under physiologic conditions, fractional sodium reabsorption by the proximal tubule varies in tandem with SNGFR (Thomson and Blantz 2008; Thomson et al. Jan 2001). Cooling at 28°C yields almost no change in proximal tubule fractional reabsorption, despite the apparent reduction in SNGFR (Broman and Källskog 1995). To maintain a constant proximal tubule fractional reabsorption as temperature varies, we apply a temperature-dependent factor $\kappa_{\text{GTB}}$, given by

$$\kappa_{\text{GTB}} = 0.700 - 0.0490 \times (T - 37.0). \quad (A34)$$

The second factor in Equation (A32) $S_{\text{PN}}(\text{RPP})$, accounts for pressure natriuresis, where proximal tubular water reabsorption decreases with increasing perfusion pressure (Sgouralis and Layton 2014)

$$S_{\text{PN}}(\text{RPP}) = 1 - 0.450 \times \left( \frac{\max(\text{RPP}, 80.0)}{100} - 1 \right). \quad (A35)$$

where RPP is in mmHg.

The model predicts luminal $[\text{Cl}^-]$ along the tubule, based on conservation of mass (Equation (3) in main text). The outflow $[\text{Cl}^-]$ is assumed to be at the site of the macula densa and is used to determine the TGF response. Maximum active transport rate $V_{\text{max}}$ (nmol/cm²/sec) along the thick ascending limb depends on temperature as follows

$$V_{\text{max}}^{\text{TAL}} = \max(0, 16.2 + 1.01 \times (T - 37.0)). \quad (A36)$$

This relation assumes negligible time lag between temperature increase and tubular transport upregulation.
Author/s:
Sgouralis, I; Evans, RG; Gardiner, BS; Smith, JA; Fry, BC; Layton, AT

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