Scalar Dark Matter and Standard Model with Four Generations

Xiao-Gang He\textsuperscript{1,2}, Shu-Yu Ho\textsuperscript{1}, Jusak Tandean\textsuperscript{1}, and Ho-Chin Tsai\textsuperscript{1}

\textsuperscript{1}Department of Physics, Center for Theoretical Sciences, and LeCosPA Center, National Taiwan University, Taipei
\textsuperscript{2}Institute of Particle Physics and Cosmology, Department of Physics, Shanghai Jiao Tong University, Shanghai

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Abstract

We consider a scalar dark matter model, the SM4+D, consisting of the standard model with four generations (SM4) and a real gauge-singlet scalar called darkon, $D$, as the weakly interacting massive particle (WIMP) dark-matter (DM) candidate. We explore constraints on the darkon sector of the SM4+D from WIMP DM direct-search experiments, including CDMSII and CoGeNT, and from the decay of a $B$ meson into a kaon plus missing energy. We find that a sizable portion of the darkon parameter space is still compatible with the experimental data. Since the darkon-Higgs interaction may give rise to considerable enhancement of the Higgs invisible decay mode, the existence of the darkon could lead to the weakening or evasion of some of the restrictions on the Higgs mass in the presence of fourth-generation quarks. In addition, it can affect the flavor-changing decays of these new heavy quarks into a lighter quark and the Higgs boson, as the Higgs may subsequently decay invisibly. Therefore we also study these flavor-changing neutral transitions involving the darkon, as well as the corresponding top-quark decay $t \to cDD$, some of which may be observable at the Tevatron or LHC and thus provide additional tests for the SM4+D.
I. INTRODUCTION

The existence of dark matter (DM) in the Universe is now widely accepted. Various observations have established that DM makes up 23% of the total cosmic energy density [1]. Despite this evidence, however, the identity of the basic constituents of DM has so far remained a mystery. It is therefore important to explore different possible DM scenarios.

One of the popular candidates for DM is the weakly interacting massive particle (WIMP). To account for WIMP DM, the standard model (SM) of particle physics needs to be enlarged. The simplest extension of the SM possessing a WIMP candidate is the SM+D, which combines the SM with a real SM-singlet scalar field \( D \), dubbed darkon, to play the role of the DM. This darkon model and some variations of it have been much studied in the literature [2–12].

In this paper we explore a somewhat enlarged darkon model we call SM4+D, which consists of the darkon and the SM extended by the inclusion of a fourth sequential generation of quarks and leptons. This SM with four generations (SM4) has received much attention in recent years [13–23]. Among the reasons [13] that have been put forward for all this interest in the SM4 are that it is not ruled out by electroweak precision tests [14–16], offers possible resolutions for certain anomalies in flavor-changing processes [17–20], and might solve baryogenesis-related problems [21]. In view of the desirable features of the model, some of which nevertheless remain open questions, it is of interest also to consider integrating the darkon field into it, assuming that the new fermions are all unstable, in which case the SM4+D is the simplest WIMP DM model in the presence of the fourth generation. As we will elaborate later, the DM sector of the SM4+D can have important implications which are absent or suppressed in the SM+D with three generations (hereafter referred to as SM3+D). In particular, now that the LHC is operational, the extra fermions could give rise to processes involving the darkon which are potentially observable after the LHC reaches full capacity in the near future.

In the next section we describe the main features of the SM4+D relevant to our study. Subsequently, after specifying the masses of the fourth-generation fermions, we extract the values of the darkon-Higgs coupling, to be used in later sections. In Sec. III we explore constraints on this darkon model from DM direct searches at underground facilities. Recently there have been a number of such searches which can provide limits on some of the parameter space of the darkon model. We proceed in Sec. IV to discuss the complementarity of DM direct-detection experiments and Higgs studies at colliders in probing the darkon properties. The simultaneous existence of the darkon and 4th-generation fermions in the SM4+D can have substantial impact on Higgs collider searches. Since ongoing and near-future DM direct-search experiments are not likely to be sensitive to darkon masses of a few GeV or less, other processes are needed to probe the model in this low-mass region. In Sec. V we consider such processes, focusing on the \( B \)-meson decay into a kaon and a pair of darkons, \( B \to KDD \), which contributes to the \( B \) decay into \( K \) plus missing energy, \( B \to KE \). There is currently experimental information on the latter decay which can be used to place restrictions on part of the darkon low-mass region. In Sec. VI we explore some implications of the new fermions for the darkon sector that are lacking or missing in the SM3+D. Specifically, we look at the Higgs-mediated flavor-changing top-quark decay \( t \to cDD \), which is very suppressed in the SM3+D and can be greatly enhanced by the new-
quark contribution, and also deal with the corresponding decays of the 4th-generation quarks. These processes may be detectable at currently running or future colliders and, if observed, could offer additional means to probe darkon masses from zero up to hundreds of GeV. We give our conclusions in Sec. VII.

Before proceeding to the next section, we would like to summarize the relic-density requirements that any WIMP candidate has to meet. For a given interaction of the WIMP with SM4 particles, its annihilation rate into the latter and its relic density \( \Omega_D \) can be calculated and are related to each other by the thermal dynamics of the Universe within the standard big-bang cosmology \[24\]. To a good approximation,

\[
\Omega_D h^2 \simeq \frac{1.07 \times 10^9 x_f}{\sqrt{g_*} m_{pl} \langle \sigma_{\text{ann}} v_{\text{rel}} \rangle \text{GeV}}, \quad x_f \simeq \ln \frac{0.038 m_{pl} m_D \langle \sigma_{\text{ann}} v_{\text{rel}} \rangle}{\sqrt{g_*} x_f},
\]

where \( h \) is the Hubble constant in units of 100 km/(s·Mpc), \( m_{pl} = 1.22 \times 10^{19} \) GeV is the Planck mass, \( x_f = m_D / T_f \) with \( T_f \) being the freezing temperature, \( g_* \) is the number of relativistic degrees of freedom with masses less than \( T_f \), and \( \langle \sigma_{\text{ann}} v_{\text{rel}} \rangle \) is the thermally averaged product of the annihilation cross-section of a pair of WIMPs into SM4 particles and the relative speed of the WIMP pair in their center-of-mass (cm) frame. Since \( \Omega_D \) is known from observations, using the above relations one can extract the allowed range of \( \sigma_{\text{ann}} \) for each value of \( m_D \).

II. BRIEF DESCRIPTION OF SM4+D

Being a WIMP DM candidate, the darkon \( D \) has to be stable against decaying into SM4 particles. This can be realized by assuming \( D \) to be a singlet under the SM4 gauge groups and introducing a discrete \( Z_2 \) symmetry into the model. Under the \( Z_2 \) transformation, \( D \rightarrow -D \), while all SM4 fields are unchanged. Requiring, in addition, that the darkon interactions be renormalizable implies that \( D \) can interact with the SM4 fields only through its coupling to the Higgs-doublet field \( H \). It follows that the general form of the darkon Lagrangian, besides the kinetic part \( \frac{1}{2} \partial^\mu D \partial_\mu D \) and the SM4 terms, can be expressed as \[2–4\]

\[
\mathcal{L}_D = -\frac{\lambda_D}{4} D^4 - \frac{m_0^2}{2} D^2 - \lambda D^2 H^\dagger H,
\]

(2)

where \( \lambda_D, m_0, \) and \( \lambda \) are free parameters, and we have followed the notation of Ref. [10]. The parameters in the potential should be chosen such that \( D \) does not develop a vacuum expectation value and the \( Z_2 \) symmetry is not broken, which will ensure that the darkon does not mix with the Higgs field, avoiding possible fast decays into other SM4 particles.

The Lagrangian in Eq. (2) can be rewritten to describe the interaction of the physical Higgs boson \( h \) with the darkon as\[1\]

\[
\mathcal{L}_D = -\frac{\lambda_D}{4} D^4 - \left( \frac{m_0^2 + \lambda v^2}{2} \right) D^2 - \frac{\lambda}{2} D^2 h^2 - \lambda v D^2 h,
\]

(3)

\[1\] Obviously, \( h \) here is not to be confused with the Hubble constant, also denoted by \( h \), in the combination \( \Omega_D h^2 \).
where \( v = 246 \text{ GeV} \) is the vacuum expectation value of \( H \). The second term in \( \mathcal{L}_D \) contains the darkon mass \( m_D = (m_0^2 + \lambda v^2)^{1/2} \), and the last term, \(-\lambda v D h\), has a major role in the determination of relic density of the darkon. Clearly this model has a small number of free parameters in its DM sector: the darkon mass \( m_D \), the Higgs-darkon coupling \( \lambda \), and the darkon self-interaction coupling \( \lambda_D \), besides the Higgs mass \( m_h \). Our analysis will not involve \( \lambda_D \).

For \( m_D < m_h \) the relic density results, at leading order, from the annihilation of a darkon pair into SM4 particles via Higgs exchange \([2–4]\), namely \( DD \to h^* \to X \), where \( X \) indicates SM4 particles. Since the darkon is cold DM, its speed is nonrelativistic, and so a darkon pair has an invariant mass \( \sqrt{s} \simeq 2m_D \). With the SM4+D Lagrangian determined, the \( h \)-mediated annihilation cross-section of a darkon pair into SM4 particles is then given by \([4]\]

\[
\sigma_{\text{ann}} v_{\text{rel}} = \frac{8\lambda^2 v^2}{(4m^2_D - m^2_h)^2 + \Gamma^2_h m^2_h} \sum_i \frac{\Gamma(\tilde{h} \to X_i)}{2m_D},
\]

where \( v_{\text{rel}} = 2|\mathbf{p}^\text{cm}_D|/m_D \) is the relative speed of the \( DD \) pair in their cm frame, \( \tilde{h} \) is a virtual Higgs boson having the same couplings to other states as the physical \( h \) of mass \( m_h \), but with an invariant mass \( \sqrt{s} = 2m_D \), and \( \tilde{h} \to X_i \) is any kinematically possible decay mode of \( \tilde{h} \). To determine \( \Sigma_i \Gamma(\tilde{h} \to X_i) \), one computes the \( h \) width and then sets \( m_h \) equal to \( 2m_D \). For \( m_D \geq m_h \), darkon annihilation into a pair of Higgs bosons, \( DD \to hh \), also contributes to \( \sigma_{\text{ann}} \), through \( s-, t-, u\)-channel, and contact diagrams with vertices arising from the last two terms of \( \mathcal{L}_D \) in Eq. (3) and the Higgs self-interaction (see, e.g., Ref. [4]). This becomes one of the leading contributions to \( \sigma_{\text{ann}} \), along with \( DD \to h^* \to WW, ZZ \), if \( m_D \gg m_{\nu,W,Z,h} \) \([3,4]\).

Compared to the SM3+D case, one effect of the fourth generation of quarks and leptons in the SM4+D is to enlarge the Higgs total width, \( \Gamma_h \), and also the total width \( \Sigma_i \Gamma(\tilde{h} \to X_i) \) of the virtual Higgs, \( \tilde{h} \). These new heavy fermions contribute to the total widths mainly via the decay modes into fermion-antifermion pairs if kinematically possible and, exclusively for the new quarks, the decay mode into a gluon pair induced by a quark loop. Needless to say, the changes caused by the presence of these fermions depend on their masses.

There are constraints on the masses of the 4th-generation fermions from currently available experimental data. The masses of the heavy charged-lepton \( \ell' \) and heavy neutrino \( \nu' \), both assumed to be unstable, have the PDG lower bounds \( m_{\ell'} > 100.8 \text{ GeV} \) and \( m_{\nu'} > 90.3 \text{ GeV} \) \([1]\). For the masses of the new up- and down-type quarks, \( t' \) and \( b' \), respectively, the strongest limits are \( m_{t'} > 311 \text{ GeV} \) and \( m_{b'} > 338 \text{ GeV} \), from searches at the Tevatron \([25]\). The mass differences between the new quarks and between the new leptons turn out to be subject to empirical constraints as well. Electroweak precision data prefer \( m_{\ell'} - m_{\nu'} \simeq [5 + \ln(m_h/115 \text{ GeV})] \times 10 \text{ GeV} \) and \( 30 \text{ GeV} \lesssim m_{\ell'} - m_{\nu'} \lesssim 60 \text{ GeV} \) \([13]\). Accordingly, for numerical work in this paper we take for definiteness \( m_{\ell'} = 200 \text{ GeV} \), \( m_{\nu'} = 150 \text{ GeV} \), \( m_{t'} = m_{b'} + 55 \text{ GeV} \), and \( m_{t'} = 500 \text{ GeV} \), but we also sometimes make comparisons with the \( m_{\ell'} = 400 \) and \( 600 \text{ GeV} \) cases. We remark that these \( m_{\nu'} \) values fall within the ranges allowed by recent global fits for the SM4 \([13,19]\), although \( m_{t'} = 600 \text{ GeV} \) is slightly above the unitarity upper-bound of \( \sim 550 \text{ GeV} \) \([13]\).

With these mass choices, we can find the Higgs total widths, which we subsequently apply in Eq. (4), combined with the \( DD \to hh \) contribution if \( m_D \geq m_h \), in order to extract the darkon-Higgs coupling \( \lambda \) for given values of \( m_D, m_h \), and \( \langle \sigma_{\text{ann}} v_{\text{rel}} \rangle \). The allowed range of \( \langle \sigma_{\text{ann}} v_{\text{rel}} \rangle \) as
a function of $m_D$ can be inferred, with the aid of Eq. (1), from the data on the relic density. Its most recent value is $\Omega_D h^2 = 0.1123 \pm 0.0035$, determined by an analysis of the seven-year data from WMAP combined with other data [26]. From this number, one can derive the 90%-C.L. range $0.1065 \leq \Omega_D h^2 \leq 0.1181$, which we adopt for our numerical study. We show in Fig. 1 the resulting ranges of $\lambda$, taken to be positive, corresponding to $3 \text{GeV} \leq m_D \leq 1 \text{TeV}$ for some specific values of the Higgs mass, which we choose to be $m_h = 115, 200, \text{and } 300 \text{GeV}$ for illustration. We present plots both in the SM3+D and in the SM4+D with $m_{t'} = 500 \text{GeV}$ for comparison purposes. The SM4+D plots for $m_{t'} = 400 \text{ and } 600 \text{GeV}$ turn out to be very similar to the one displayed.

There are several points worth pointing out in relation to what can be seen in Fig. 1. First, although only a relatively narrow range of the DM relic density is allowed, evidently it can be fairly easily reproduced in both the SM3+D and SM4+D. Second, $\lambda$ is not small for the lower values of $m_D$, and this will result in a considerable branching ratio of the Higgs invisible decay mode in the two models, as we will discuss further later. Third, for $3 \text{GeV} \leq m_D \lesssim 5 \text{GeV}$ the size of $\lambda$ can exceed unity and the $m_h = 300 \text{GeV}$ curve approaches 3 at $m_D \sim 3 \text{GeV}$. This may seem to signal the breakdown of perturbativity in the low-$m_D$ range, but an investigation into the perturbative unitarity of darkon-Higgs interactions at tree level [6] has come up with the limit $|\lambda| < 4\pi \simeq 12.6$. Furthermore, it has been suggested in Ref. [7] that, due to a lack of clear division between the perturbative and nonperturbative regions of the parameter space, a reasonable requirement is $|\lambda| < 2\sqrt{\pi} (m_h/100 \text{GeV})^2$, which is roughly comparable to the preceding limit for the Higgs masses we have picked. Fourth, although the $\lambda$ values tend to become small as $m_D$ enters the region between 50 and 200 GeV or so, they get large again, approximately linearly with $m_D$, as $m_D$ grows sufficiently large. This follows from the facts that $\langle \sigma_{\text{ann}} v_{\text{rel}} \rangle$ is roughly constant for the $m_D$ range of interest and that $\sigma_{\text{ann}} v_{\text{rel}} \simeq \lambda^2/(4\pi m_D^2)$ for $m_D \gg m_{W,Z,h,t}$ [3, 4, 10]. Lastly, the curves in the SM4+D appear quite similar to the corresponding ones in the SM3+D, but at most of the $m_D$ values considered we find the former to be lower than the latter. This decrease is mainly less than 20%, but it reaches nearly 25%.

![FIG. 1: Darkon-Higgs coupling $\lambda$ as a function of darkon mass $m_D$ for Higgs mass values $m_h = 115, 200, 300 \text{GeV}$ in (a) SM3+D and (b) SM4+D with $m_{t'} = 500 \text{GeV}$. The band widths in all figures correspond to the relic-density range which we have taken, $0.1065 \leq \Omega_D h^2 \leq 0.1181$.](image)
at $m_D \sim 60$ GeV. The reason for the decrease is that the Higgs total width in the SM4 is, as mentioned earlier, enlarged relative to that in the SM3, which is also true for the total width of $\tilde{h}$ in Eq. (4). The enlargement ranges mostly from a few percent to $\sim 40\%$ and gets as high as $\sim 70\%$ at $m_h = 2m_D \sim 120$ GeV.

### III. CONSTRAINTS FROM DARK-MATTER DIRECT SEARCHES

A number of underground experiments have been and are being performed to detect DM directly by looking for the recoil energy of nuclei caused by the elastic scattering of a WIMP off a nucleon [27–32]. Although indirect DM searches have recently turned up some intriguing results which may be interpreted as evidence for WIMPs [33], it is very difficult to establish a firm connection to DM due to the indirect nature of the observed events. Therefore, direct detection is crucial to determine the properties of DM.

In the SM4+D, the WIMP-nucleon interaction occurs via the exchange of a Higgs boson between the darkon and the nucleon $N$ in the $t$-channel process $DN \rightarrow DN$. Thus to evaluate this elastic scattering requires knowing not only the darkon-Higgs coupling $\lambda$, but also the Higgs-nucleon coupling $g_{NNh}$, which parametrizes the Higgs-nucleon interaction described by $L_{NNh} = -g_{NNh} \bar{N}N h$. From this Lagrangian and $L_D$ in Eq. (3), one can derive for $|t| \ll m_h^2$ the darkon-nucleon elastic cross-section [2–4, 8, 9]

$$\sigma_{el} \simeq \frac{\lambda^2 g_{NNh}^2 v^2 m_N^2}{\pi (m_D + m_N)^2 m_h^4},$$

having used the approximation $(p_D + p_N)^2 \simeq (m_D + m_N)^2$.

It remains to determine the value of $g_{NNh}$, which is related to the underlying Higgs-quark interaction described by $L_{qqh} = -\sum_q m_q \bar{q}q h/v$, where in the SM4 the sum runs over the eight quark flavors, $q = u, d, s, c, b, t, b', t'$. Since the energy transferred in the darkon-nucleon scattering is very small, of order tens of keV, one can employ a chiral-Lagrangian approach to estimate $g_{NNh}$. This has been done previously in the context of the SM3 [9, 34, 35]. In the SM4 case, we modify the derivation described in Ref. [9], incorporating the $t'$ and $b'$ contributions, to arrive at

$$g_{NNh}^{\text{SM4}} = \frac{m_N - \frac{17}{27} m_B}{v},$$

where $m_N$ is the nucleon mass and $m_B$ denotes the lightest octet-baryon mass in the chiral limit, which can be related to the pion-nucleon sigma term, $\sigma_{\pi N}$, by $m_B \simeq -13.39 \sigma_{\pi N} + 1.269$ GeV [9]. With $\sigma_{\pi N} = 45$ MeV [36], we obtain

$$g_{NNh}^{\text{SM4}} = 2.11 \times 10^{-3},$$

to be compared with the SM3 value $g_{NNh}^{\text{SM3}} = 1.71 \times 10^{-3}$ [9]. We adopt these numbers in our numerical calculations below. We note, however, that $\sigma_{\pi N}$ is not well determined, with values ranging roughly from 35 MeV to 80 MeV having been quoted in the literature [37–39], which translate into $1.8 \times 10^{-3} \lesssim g_{NNh}^{\text{SM4}} \lesssim 3.3 \times 10^{-3}$ and $1.3 \times 10^{-3} \lesssim g_{NNh}^{\text{SM3}} \lesssim 3.2 \times 10^{-3}$. 
With $\lambda$ and $g_{NNh}$ known, we can now predict the darkon-nucleon elastic cross-section $\sigma_{el}$ as a function of darkon mass once the Higgs mass is specified. We show our results for $\sigma_{el}$ in Fig. 2 where the choices of darkon and Higgs masses are the same as those in Fig. 1. For comparison, we display $\sigma_{el}$ graphs in the SM3+D and in the SM4+D with $m_{t'} = 500$ GeV. The SM4+D plots for $m_{t'} = 400$ and 600 GeV are again similar to the one displayed. We find that at most of the $m_D$ values considered the $\sigma_{el}$ curves in the SM4+D for a fixed $m_h$ are higher than the corresponding ones in the SM3+D. This difference ranges from a few to roughly 50 percent and results from the $g_{NNhh}^{SM4}$ enhancement relative to $g_{NNhh}^{SM3}$ overcoming the $\lambda_{SM4+D}$ suppression relative to $\lambda_{SM3+D}$ mentioned in the preceding section.

FIG. 2: Darkon-nucleon elastic cross-section $\sigma_{el}$ as a function of darkon mass $m_D$ for Higgs mass values $m_h = 115, 200, 300$ GeV in (a) SM3+D and (b) SM4+D with $m_{t'} = 500$ GeV, compared to 90%-C.L. upper limits from XENON10 (black dashed-curve), CDMS II (brown [gray] dashed-curve), and CoGeNT (purple dashed-curve), as well as projected sensitivities of SuperCDMS at Soudan (green dot-dashed curve), SuperCDMS at Snolab (brown [gray] dotted curve), and XENON100 (black dotted curve).
In Fig. 2, we also plot the 90%-C.L. upper-limit curves for the WIMP-nucleon spin-independent elastic cross-section reported by the XENON10 [28], CDMS II [30], and CoGeNT [31] experiments, along with the expected sensitivities of a number of future experiments [38]. For $m_D \lesssim 10$ GeV, there are also limits from CRESST-I [27] and TEXONO [29], but they are both above the predictions of the two models.

Comparing the prediction curves of both models to the experimental upper-bounds in Fig. 2, one can see that some portions of the darkon mass regions considered are excluded, but the greater part of them are still viable. More precisely, for $m_h = 115, 200, \text{ and } 300$ GeV the XENON10 and CDMS II limits have ruled out darkon masses from $\sim 9$ GeV to between 70 and 80 GeV, except for the $50 \text{ GeV} < m_D < 70$ GeV range in the $m_h = 115$ GeV case. Moreover, in the low-$m_D$ sections of the plots the exclusion limit from CoGeNT can be seen to rule out part of the $4 \text{ GeV} \lesssim m_D \lesssim 5$ GeV range. In contrast, darkon masses larger than 80 GeV or so are not yet probed by the current data from direct searches. As the projected sensitivities of future experiments in this figure suggest, SuperCDMS at Snolab and XENON100 may probe these models further to $m_D \sim 400$ GeV, but SuperCDMS at Soudan may be unlikely to provide much stronger constraints on the models than the present bounds.

It is interesting to point out that these two darkon models can accommodate the possibility that the excess events observed by CoGeNT originate from interactions with a relatively light WIMP of mass between 7 and 11 GeV [31], which is compatible with the two signal-like events detected by CDMS II [30] if they are also interpreted as evidence for WIMP interactions. For $m_D$ values within this range, the prediction curves in Fig. 2 each have some overlap with the possible signal region reported by CoGeNT [31]. This is more so if we take into account the uncertainties in $g_{NNh}$ noted above, which could imply an increase in the predicted $\sigma_{el}$ by up to a factor of 3.

Before moving on, it is worth remarking that, as Fig. 2 indicates, $\sigma_{el}$ for a fixed $m_h$ approaches a constant value as $m_D$ becomes much greater than $m_{W,Z,h,t}$. The reason is that in this large-$m_D$ limit the ratio $\lambda^2/m^2_D$ is, as pointed out in the preceding section, approximately constant and $\sigma_{el}$ in Eq. (5) is proportional to the same ratio, $\lambda^2/m^2_D$. Another observation from this figure is that the asymptotic value of $\sigma_{el}$ decreases as $m_h$ increases, which is in accord with Eq. (5). Hence direct DM searches in the future may lack the sensitivity to probe the larger darkon masses if the Higgs mass is also large.

IV. SOME IMPLICATIONS FOR HIGGS SEARCHES AT COLLIDERS

Since both the SM3+D and SM4+D have only a small number of free parameters, the relevant ones here being $\lambda$, $m_D$, and $m_h$, it is possible to draw strong correlations among them [10]. This implies that these darkon models have a high degree of predictivity and that there is some simplification in testing them, without requiring many different observables. To illustrate this, we now discuss the Higgs decay into a pair of darkons, $h \rightarrow DD$, and some of its consequences for Higgs studies at colliders, in light of the bounds obtained above from comparing with DM direct-detection data.
Using the \( \lambda \) values obtained in Sec. III we compute the rate and branching ratio of the invisible mode \( h \to DD \). The results are depicted in Fig. 3 where the Higgs and darkon mass choices are the same as those in Fig. 1. One can observe that the situations in the SM3+D and SM4+D are similar, namely that the sizable values of \( \lambda \) in Fig. 1 translate into huge enhancement of the Higgs width via the additional process \( h \to DD \) and, consequently, an invisible branching ratio that is large. This is especially so if \( 2m_D < m_h < 2m_W \), in which case the Higgs partial width into standard particles is small. Although the 4th-generation quarks can cause the decay mode into a gluon pair, \( h \to gg \), to dominate if \( m_h \lesssim 140 \text{ GeV} \) [15], the inclusion of the darkon in the SM4+D leads to the dominance of \( h \to DD \) instead.

The potential importance of the Higgs invisible decay mode in the darkon presence can alleviate some of the restrictions on Higgs masses in the SM4. For instance, at hadron colliders the important channel \( gg \to h \to WW \to \ell\nu\ell\nu \) is expected to be enhanced due to the new quarks in the SM4 by a factor of 9 for \( 100 \text{ GeV} \lesssim m_h \lesssim 200 \text{ GeV} \), the measurement of which would also provide indirect evidence for the new quarks [13]. Preliminary searches at the Tevatron for this channel have so far come back negative, thus excluding a large portion of this \( m_h \) range in the SM4 [13, 39]. In the SM4+D, however, the possible dominance of the \( h \to DD \) mode implies that the enhancement of \( gg \to h \to WW \to \ell\nu\ell\nu \) would likely be reduced or even negated completely, and so the Higgs-mass constraints could be weakened or evaded.

**FIG. 3**: Partial width and branching ratio of invisible decay \( h \to DD \) as functions of darkon mass \( m_D \) for Higgs mass values \( m_h = 115, 200, 300 \text{ GeV} \) in (a,c) SM3+D and (b,d) SM4+D with \( m_\nu = 500 \text{ GeV} \).
As discussed previously \[10\], collider measurements of the Higgs invisible decay with sufficient precision can lift some possible ambiguities in determining the darkon mass from direct DM searches. A substantial Higgs invisible decay can also be advantageous for testing the darkon models if the constraints from direct DM searches are combined with Higgs studies at colliders. As found above, the greater part of the darkon mass range from about 9 to 80 GeV in the SM3+D and SM4+D have been ruled out by direct-detection data if the Higgs mass \( m_h = 115, 200, \) or 300 GeV, the main exception being the neighborhood of \( m_D \sim 57.5 \) GeV. Since Fig. 3 shows that a Higgs boson with one of these masses decays dominantly or significantly into a darkon pair if \( m_D \lesssim 50 \) GeV, then the observation of such a Higgs boson with a sizable invisible branching-ratio might hint at inconsistencies of the models. All this illustrates that the interplay between direct DM searches and the study of the Higgs boson at colliders can yield crucial information about the darkon properties.

An enhanced \( B(h \rightarrow DD) \) affects not only collider searches for the Higgs boson, but also decays which are mediated by or produce it. In the following two sections, we deal with such processes arising from the Higgs flavor-changing neutral couplings to quarks.

V. CONSTRAINTS FROM \( B \rightarrow KDD \) DECAYS

As seen in Sec. III, direct DM searches with underground detectors currently being done or to be done in the near future are not expected to be sensitive to darkon masses below a few GeV. It turns out that such darkon masses can be probed using the decays of mesons containing the \( b \) quark. In this section we explore constraints available from the \( B \)-meson decay \( B \rightarrow KDD \), which contributes to the \( B \) decay into \( K \) plus missing energy, \( B \rightarrow K \bar{\nu}E \). One could carry out a similar analysis using \( B \rightarrow K^*DD \), but we will not do so here. We will also briefly comment on the spin-one bottomonium decay \( \Upsilon \rightarrow DD\gamma \).

Since the Higgs boson \( h \) is the only SM particle to which \( D \) couples, \( B \rightarrow KDD \) is induced by the flavor-changing \( b \)-quark decay \( b \rightarrow sh^* \rightarrow sDD \), the effective \( bsh \) coupling being loop-generated with up-type quarks and the \( W \) boson in the loops. These transitions have been studied previously in the context of the SM3+D in Refs. \[7, 12\]. Generalizing their results to the SM4+D, we can express the effective Hamiltonian for \( b \rightarrow sh^* \rightarrow sDD \) as

\[
\mathcal{H}_{b \rightarrow sDD} = \frac{\lambda g_{bs}}{2m_h^2} \bar{s}(1 + \gamma_5) b D^2 ,
\]

where

\[
g_{bs} = \frac{3g^2}{64\pi^2}\left(\lambda^b_t x_t + \lambda^b_{t'} x_{t'}\right) , \quad x_q = \frac{m_q^2}{m_W^2} , \quad \lambda^b_q = V_{qs}V_{qb} ,
\]

with \( V_{kl} \) being the elements of the 4×4 Cabibbo-Kobayashi-Maskawa (CKM4) matrix, and contributions from \( u \) and \( c \) quarks have been neglected. Hence the corresponding expression for \( g_{bs} \) in the SM3+D does not contain the \( \lambda^b_{t'} x_{t'} \) term.
The amplitude for $B^- \to K^- DD$ is then
\[
\mathcal{M}(B^- \to K^- DD) = \frac{\lambda g_{bs} m_B^2}{m_h^2} f_0(\hat{s}) , \tag{10}
\]
where $f_0(\hat{s}) = 0.3 \exp(0.63 \hat{s}/m_B^2 - 0.095 \hat{s}^2/m_B^4 + 0.591 \hat{s}^3/m_B^6)$ is the relevant $B \to K$ form-factor \cite{[7]}, with $\hat{s} = (p_B - p_K)^2$, and the approximation $(m_B^2 - m_K^2)/(m_b - m_\ell) \approx m_B^2/m_b$ has been made. It follows that
\[
\Gamma(B^+ \to K^+ DD) = \frac{\lambda^2 |g_{bs}|^2 m_B}{m_h^4} \frac{I(m_D)}{512 \pi^3} , \tag{11}
\]
where a factor of 1/2 has been included to account for the identical $D$’s in the final state and
\[
I(m_D) = \int_{4m_D^2}^{(m_B - m_K)^2} d\hat{s} \left(f_0(\hat{s})\right)^2 \sqrt{1 - \frac{4m_D^2}{\hat{s}}} \sqrt{(m_B^2 - m_K^2 - \hat{s})^2 - 4m_K^2 \hat{s}} . \tag{12}
\]
We note that our formula for the $B \to KDD$ rate agrees with the corresponding one obtained in Ref. \cite{[12]}, but is 4 times smaller than that given in Ref. \cite{[7]}\footnote{This can be traced to a factor of 1/2 apparently missing in the expression for the $B \to KDD$ amplitude in the Eq. (6) of the first paper in Ref. \cite{[7]}.}. Since for $m_D \ll m_h$ we can simplify Eq. (11) to
\[
\sigma_{ann} v_{rel} \simeq \frac{\lambda^2 |g_{bs}|^2}{m_h^4} \frac{4\pi^2 \sum_i \Gamma(\hat{h} \to X_i)}{m_D} , \tag{13}
\]
we can rewrite Eq. (11) as
\[
\Gamma(B^+ \to K^+ DD) \simeq \frac{|g_{bs}|^2 m_B I(m_D)}{2048 \pi^3 v^2} \frac{\left(\sigma_{ann} v_{rel}\right) m_D}{\sum_i \Gamma(\hat{h} \to X_i)} , \tag{14}
\]
where both $\sigma_{ann} v_{rel}$ and $\sum_i \Gamma(\hat{h} \to X_i)$ have $m_D$ dependence. We can get constraints on the parameter space $m_D \leq (m_B - m_K)/2$ by comparing this prediction with the experimental information on the $B$ decay into a kaon plus missing energy, which receives contributions from $B \to KDD$ and $B \to K\nu\bar{\nu}$. We first update the constraints in the SM3+D and then discuss the SM4+D case.

The prediction of the branching ratio $B(B \to KDD)$ in the SM3+D using Eq. (14), with the $\lambda^{bs} x_{\ell}$ term in $g_{bs}$ dropped, involves large uncertainties which come mainly from the calculation of the total width $\sum_i \Gamma(\hat{h} \to X_i)$ for $m_\hat{h}$ under a few GeV. In the case of the physical $h$, for $m_\hat{h} \lesssim 2$ GeV the predicted rate of the important channel $h \to$ hadrons is well known to contain significant uncertainties \cite{[40],[41]}. In estimating the $\hat{h}$ total width, for $2m_\pi \leq m_\hat{h} \leq 1.4$ GeV we adopt the $\Gamma(h \to$ hadrons) results from Ref. \cite{[41]}, whereas for smaller and larger values of $m_\hat{h}$ we simply use the perturbative formulas for Higgs decays \cite{[42]}. We graph the resulting $B(B \to KDD)$ as a function of $m_D$ in Fig. \ref{fig:bdkdd}, which is to be compared with experimental data.
The latest experimental search for the decay $B^+ \to K^+ \nu \bar{\nu}$ has produced the branching-ratio limit $\mathcal{B}_{\text{exp}}(B^+ \to K^+ \nu \bar{\nu}) < 14 \times 10^{-6}$ [43]. On the theoretical side, the most recent calculations in the SM3 predict $\mathcal{B}(B^+ \to K^+ \nu \bar{\nu})$ to be between $3.6 \times 10^{-6}$ and $5.1 \times 10^{-6}$, with errors of order 15% [44]. Accordingly, it is reasonable to take $\mathcal{B}(B^+ \to K^+ \nu \bar{\nu}) \simeq \mathcal{B}_{\text{exp}}(B^+ \to K^+ \nu \bar{\nu})$ in order to require that $\mathcal{B}(B^+ \to K^+ DD) < 1 \times 10^{-5}$ in the SM3+D.

We can see from Fig. 4 that the predicted $\mathcal{B}(B^+ \to K^+ DD) > 1 \times 10^{-5}$ for $m_D \lesssim 1.5$ GeV. Recalling the hadronic uncertainties mentioned above, we can then conclude that in the SM3+D much of this range of $m_D$ values, especially $m_D \lesssim 0.4$ GeV, is excluded by the data. We would need improved data from future measurements of $B \to KE$ before we could disallow more darkon masses within the $m_D < 2.4$ GeV region. These conclusions are similar to those made in Ref. [7] due partly to the stronger experimental limit at present and partly to the overestimate of their $\mathcal{B}(B \to KDD)$.

In the SM4+D, the prediction for $\Gamma(B \to KDD)$ is modified due to the presence of the new quarks, $t'$ and $b'$. The loop-induced effective coupling $g_{bs}$ in Eq. (14) receives a $t'$-quark contribution as given in Eq. (9). To examine its effect on $\Gamma(B \to KDD)$, we need to compare $g_{bs}^{\text{SM4}}$ to $g_{bs}^{\text{SM3}}$. For concreteness, we take the relevant CKM4 elements extracted in Ref. [19] from a global fit for the SM4. Accordingly, we can expect that the numbers we use are typical values for the model. Thus, with $\lambda_i^{bs} = 0.04$ in $g_{bs}^{\text{SM3}}$, we find $|g_{bs}^{\text{SM4}} / g_{bs}^{\text{SM3}}|^2$ for $m_{t'} = 400$ and 500 GeV to be similar in value, $\sim 1.2$, but it goes up to 1.6 for $m_{t'} = 600$ GeV. In addition, the presence of $t'$ and $b'$ affects the total width $\Sigma_i \Gamma(\tilde{h} \to X_i)$ in Eq. (14) mainly via their contributions to $\tilde{h} \to \text{hadrons}$ due to the quark-loop induced $\tilde{h} \to gg$, as already mentioned earlier. Despite the hadronic uncertainties, this implies that the enhancement of the $\tilde{h}$ total width in the SM4 compared to the SM3 can be expected to be less than $(5/3)^2 \simeq 2.8$ if $2m_{\pi} \leq m_{\tilde{h}} \leq 2m_{c}$, where 5 and 3 are the numbers of heavy quarks in the two models, respectively, for this $m_{\tilde{h}}$ range. This enhancement decreases to no more than 25% after the $\tilde{h} \to c\bar{c}$ channel is open. We can then conclude that the effects of these two factors on $\Gamma(B \to KDD)$ in the SM4+D amount to changes to the rate in the SM3+D by no more than a factor of 2 in either direction, implying that the curve in Fig. 4 would not be very different in the SM4+D. Since the prediction for $\mathcal{B}(B^+ \to K^+ \nu \bar{\nu})$ is
raised by at most 20% in the SM4, the empirical bound on $B(B \to KDD)$ in the SM4+D can be taken to be unchanged compared to that in the SM3+D. It follows that the constraints on the darkon masses within the $m_D < 2.4$ GeV range in the SM4+D are similar to those in the SM3+D.

We should also mention that for $m_D \lesssim 170$ MeV an additional restriction is provided by the kaon decay $K^+ \to \pi^+E$, which receives a contribution from $K^+ \to \pi^+DD$. The agreement between the SM3 expectation and experimental data on $K^+ \to \pi^+E$ implies that for $m_D < \sim 170$ MeV the SM3+D is already ruled out, as is the SM4+D. This is consistent with what can be inferred from the low-$m_D$ end of Fig. 4.

For the larger range $m_D < \sim 5$ GeV, there may also be constraints available from future measurements of the decays $\Upsilon \to DD\gamma$. Presently, the existing experimental limits on $\Upsilon \to \gamma+$invisible are not yet strong enough to probe these darkon models.

VI. FCNC DECAYS $Q \to qDD$

The presence of the new quarks in the SM4+D can have important implications for probing the darkon sector that are lacking or absent in the SM3+D. In the SM3 the flavor-changing neutral current (FCNC) top-quark decay $t \to ch$ is known to be very suppressed, with a branching ratio estimated to be between $10^{-15}$ and $10^{-13}$, but in the SM4 the branching ratio can be enhanced by several orders of magnitude. We expect that in the SM4+D the related decay $t \to ch^* \to cDD$, if kinematically allowed, can be similarly enhanced. These processes may be detectable at the LHC after its operation reaches full capacity in the near future. The Tevatron and the LHC can also produce the new quarks, $t'$ and $b'$, if they exist, in a similar way as they can produce the $t$ quark, albeit fewer of them due to their bigger masses. It is therefore of interest as well to explore their FCNC decays, $t' \to (c, t)h^* \to (c, t)DD$ and $b' \to (s, b)h^* \to (s, b)DD$, which may have observable rates. These decays could, in principle, probe darkon masses from zero all the way up to $(m_Q - m_q)/2$, hence covering potentially wider $m_D$ ranges than those covered by some of the DM direct searches in the future. Here we estimate the branching ratios of these FCNC decays involving the darkon. The corresponding decays with the $u$ and $d$ quarks, $t' \to uDD$ and $b' \to dDD$, are comparatively suppressed due to the less favorable CKM4 factors.

The Lagrangian describing the FCNC transition $Q \to qh$ involving a heavy quark $Q$ and a lighter quark $q$ can be written as

$$L_{Qqh} = \bar{q}(g_{QL}^QP_L + g_{QR}^QP_R)Qh,$$

where $P_{LR} = \frac{1}{2}(1 \mp \gamma_5)$ and the loop-induced couplings $g_{QL}^q, g_{QR}^q$ generally depend not only on the internal quark (and $W$) masses and the CKM matrix elements, but also on the masses and momenta of the external particles. The amplitude for $Q \to qh^* \to qDD$ is then

$$\mathcal{M}(Q \to qDD) = \frac{2\lambda v \bar{q}(g_{QL}^QP_L + g_{QR}^QP_R)Q}{m_h^2 - \bar{s} - i\Gamma_h m_h},$$

13
where $\bar{s} = (p_Q - p_q)^2$. This yields the decay rate

$$
\Gamma(Q \to qDD) = \frac{\lambda^2 v^2}{256\pi^3 m_Q^3} \int_{4m_b^2}^{(m_Q - m_q)^2} \frac{ds}{s} \sqrt{1 - \frac{4m_D^2}{s}} \sqrt{(m_Q^2 - m_q^2 - \bar{s})^2 - 4m_q^2\bar{s}} \times \frac{|g_L^{Qq}|^2 + |g_R^{Qq}|^2}{4} \left( m_Q^2 + m_q^2 - \bar{s} \right) + 4 \text{Re}(g_L^{Qq}g_R^{Qq})m_qm_q
$$

$$
\left( \bar{s} - m_h^2 \right)^2 + \Gamma_h^2 m_h^2
$$

(17)

For $2m_D < m_h < m_Q - m_q$, the Higgs-pole contribution dominates this integral, and so one has $\Gamma(Q \to qDD) \simeq \Gamma(Q \to qh) B(h \to DD)$.

The effective couplings $g_{L,R}^{Qq}$ in the SM have been evaluated previously for arbitrary values of the external and internal masses \cite{47,49}. We make use of the formulas provided in Ref. \cite{49}. In our numerical illustration below, we take $m_h = 115$ GeV and $m_{t'} = 500$ GeV, as well as the corresponding elements of the CKM4 matrix extracted from a global fit in Ref. \cite{19}. To determine the branching ratios, we normalize the decay rates according to

$$
B(t \to cDD) = \frac{\Gamma(t \to cDD)}{\Gamma(t \to bW)} ,
$$

(18)

$$
B(t' \to qDD) = \frac{\Gamma(t' \to qDD)}{\Gamma(t' \to bW) + \Gamma(t' \to sW)} ,
$$

(19)

$$
B(b' \to qDD) = \frac{\Gamma(b' \to qDD)}{\Gamma(b' \to tW) + \Gamma(b' \to cW)} ,
$$

(20)

following Ref. \cite{19} in the $Q \to qh$ cases. We display the results in Fig. 5.

Estimates suggest that $t \to ch$ can be detected at the LHC if its branching ratio is several times $10^{-5}$ or higher \cite{46}. In the presence of the darkon, if $h \to DD$ is leading, $t \to ch \to cDD$ is more likely to occur than other $t \to ch \to cX$ modes. In that case, however, as Fig. 5 indicates, $B(t \to cDD) \lesssim 1.0 \times 10^{-8}$ and so $t \to cDD$ probably will not be observable in the near future. The branching ratio could be several times higher if $m_{t'} \sim 700$ GeV, but this already exceeds the perturbative unitarity upper-bound $m_{t'} \sim 550$ GeV \cite{13}.

\begin{figure}[h]
\centering
\begin{subfigure}{0.45\textwidth}
\includegraphics[width=\textwidth]{plot1.png}
\caption{(a) $t \to cDD$, $t' \to cDD$, and $t' \to tDD$ as functions of darkon mass $m_D$ for Higgs mass $m_h = 115$ GeV in SM4+D with $m_{t'} = 500$ GeV.}
\end{subfigure}
\hfil
\begin{subfigure}{0.45\textwidth}
\includegraphics[width=\textwidth]{plot2.png}
\caption{(b) $b' \to sDD$ and $b' \to bDD$ as functions of darkon mass $m_D$ for Higgs mass $m_h = 115$ GeV in SM4+D with $m_{t'} = 500$ GeV.}
\end{subfigure}
\caption{Branching ratios of (a) $t \to cDD$, $t' \to cDD$, and $t' \to tDD$ and (b) $b' \to sDD$ and $b' \to bDD$ as functions of darkon mass $m_D$ for Higgs mass $m_h = 115$ GeV in SM4+D with $m_{t'} = 500$ GeV.}
\end{figure}
In contrast, the \( t' \) and \( b' \) numbers in Fig. 5 are much greater: 
\[
B(t' \to cDD) \lesssim 8.2 \times 10^{-5},
\]
\[
B(t' \to tDD) \lesssim 1.4 \times 10^{-3},
\]
\[
B(b' \to sDD) \lesssim 3.1 \times 10^{-4},
\]
and 
\[
B(b' \to bDD) \lesssim 3.3 \times 10^{-3}.
\]
Since \( t' \to qh \) and \( b' \to qh \) decays with branching ratios between \( 10^{-4} \) and \( 10^{-2} \) are expected to be within the reach of the LHC [19, 47], we may expect that these \( t' \to qDD \) and \( b' \to qDD \) decays would also be detectable at the LHC despite their final states involving missing energy.

Once they are measured, comparing the results with those from DM direct searches could provide additional consistency tests for the darkon models.

VII. CONCLUSIONS

We have explored one of the simplest dark-matter models, the SM4+D, consisting of the standard model with four generations and a real gauge-singlet scalar, the darkon, to play the role of WIMP dark matter. This model possesses not only the phenomenologically interesting features of the SM4, but also a high degree of predictivity in its DM sector. We have investigated constraints on the SM4+D from DM direct-search experiments and from \( B \)-meson decay into a kaon plus missing energy. Compared to the SM3+D case, the resulting bounds in the SM4+D are similar, namely that for the representative Higgs masses chosen most of the darkon masses between roughly 4 to 80 GeV are excluded by the direct searches and that much of the mass region below 1.5 GeV is also excluded by the \( B \) decay data. Interestingly, the SM4+D as well as the SM3+D can also accommodate the possible interpretation that the excess events recently measured by the CDMS II and CoGeNT experiments were due to interactions with a light WIMP of mass around 9 GeV. Darkon masses greater than 80 GeV in the two models are still viable and can be probed by future direct searches.

We have discussed the complementarity of DM direct searches and Higgs studies at colliders in testing the darkon sector of the SM4+D. This can be crucial for a relatively light Higgs boson, which may decay substantially into the invisible darkons. Accordingly, we have pointed out that existence of the darkon could lead to the weakening or evasion of some of the restrictions on the Higgs mass in the presence of fourth-generation fermions.

We have considered some implications of the SM4+D that are lacking or absent in the SM3+D as far as probing the darkon properties is concerned. In particular, we have examined the Higgs-mediated FCNC decays \( t \to cDD, \ t' \to (c,t)DD, \) and \( b' \to (s,b)DD, \) which may have observable rates at current or future colliders. These processes promptly proceed from the \( Q \to qh \) transitions if the decay mode \( h \to DD \) is dominant. Although the \( t \to cDD \) branching-ratio is enhanced by several orders of magnitude compared to that in the SM3+D, reaching the \( 10^{-8} \) level, this decay is still unlikely to be measurable in the near future. In contrast, the branching ratios of \( t' \to qDD \) and \( b' \to qDD \) can be as large as a few times \( 10^{-3} \), which may be detectable at the LHC. If observed, they would offer extra means to test the models, covering darkon masses from zero up to hundreds of GeV.
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