AGRICULTURAL LAND CLASSIFICATION BASED ON STATISTICAL ANALYSIS OF FULL POLARIMETRIC SAR DATA

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ABSTRACT:

The discrimination capability of Polarimetric Synthetic Aperture Radar (PolSAR) data makes them a unique source of information with a significant contribution in tackling problems concerning environmental applications. One of the most important applications of these data is land cover classification of the earth surface. These data type, make more detailed classification of phenomena by using the physical parameters and scattering mechanisms. In this paper, we have proposed a contextual unsupervised classification approach for full PolSAR data, which allows the use of multiple sources of statistical evidence. Expectation-Maximization (EM) classification algorithm is basically performed to estimate land cover classes. The EM algorithm is an iterative algorithm that formalizes the problem of parameters estimation of a mixture distribution. To represent the statistical properties and integrate contextual information of the associated image data in the analysis process we used Markov random field (MRF) modelling technique. This model is developed by formulating the maximum posteriori decision rule as the minimization of suitable energy functions. For select optimum distribution which adapts the data more efficiently we used Mellin transform which is a natural analytical tool to study the distribution of products and quotients of independent random variables. Our proposed classification method is applied to a full polarimetric L-band dataset acquired from an agricultural region in Winnipeg, Canada. We evaluate the classification performance based on kappa and overall accuracies of the proposed approach and compared with other well-known classic methods.

1. INTRODUCTION

Polarimetric Synthetic Aperture Radar (PolSAR) data remote sensing has a significant contribution in tackling problems concerning environmental applications. It is mainly because, such data are available with any weather conditions and the useful radiometric and geometric information which these data are contained. The number of studies and applications involving polarimetric SAR data is increasing steadily (J. S. Lee and Pottier 2009). These data are formed by sending and receiving the electromagnetic signal in both horizontal and vertical polarization and thus, they may carry a larger amount of information than that available from a single band. Though there is currently no sensor operating in different bands and polarizations, studies in this area are useful. In addition, the discrimination capability of PolSAR data can make them a unique source of information. One of the most important applications of these data is land cover classification of different phenomena of the earth surface (Lim et al. 1989)(Hoekman, Vissers, and Tran 2011).

Classification of PolSAR data is an important and continually developing issue for automatic analysis of land covers mapping. Compared to single polarization measurement, more detailed classification of objects and phenomena can be expanded by using the physical parameters and scattering mechanisms (Hoekman, Vissers, and Tran 2011). Various strategies of supervised and unsupervised have been proposed for classification of optical and radar remote sensing data. Supervised methods need a priori information about the classes of interest, while unsupervised approaches work on pixel or the feature vector directly extracted from original data with any knowledge. Although many advanced approaches have been proposed for classifying of SAR data (Alberga 2007), there is still a lack of studies concerning statistical properties of PolSAR data to be modelled for an efficient classification. Numerous classification methods have been proposed in the literature such as region based (Wu et al. 2008), thresholding methods (J.-S. Lee, Grunes, and Kwok 1994), model based segmentation (Lombardo et al. 2003), object based technique (Corr et al. 2003) and multi-resolution techniques (Benz et al. 2004).

In this study, we have proposed a contextual unsupervised classification approach for full PolSAR data, which allows the use of multiple sources of statistical evidence, i.e., the context, texture and a specific probability density function. These parameters and information can reflect the heterogeneity of the targets. Then Expectation-Maximization (EM) classification algorithm is performed to estimate the class parameters and classifying the PolSAR images. The EM algorithm is an iterative algorithm that formalizes the problem of parameters estimation of a mixture distribution (Zhang, Brady, and Smith 2001). This algorithm has three steps, first is the initialization for defining equally probable proportions. Second step is the E-STEP, which updates the posterior probabilities of each pixel and finally M-STEP updates the parameters estimation. In this research we used three different strategies to initialize the main EM classification method. Random initialization, H/alpha classification (Ferro-Famil, Pottier, and Lee 2001) map and

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primary classification map which produced by Mellin transform (Anfinsen and Eltoft 2011) are these initialization techniques. To represent the statistical properties and integrate contextual information of the associated image in the analysis process we used Markov random field (MRF) modelling. MRFs represent a general family of stochastic models that allow both contextual information and pixel-wise information sources to be integrated in Bayesian image processing (Li 2009). This model is developed by formulating the maximum posteriori decision rule as the minimization of suitable energy functions.

In the rest part of this paper, we first introduce EM classification method, and then principals of MRF models and Mellin transform are presented. Finally implementation of our approach on real full PolSAR data, results and discussion conclude this paper.

2. METHODOLOGY

Overall flowchart of our proposed method for unsupervised classification of PolSAR data is presented in figure 1. In the continuation more details of several steps is introduced.

2.1 EM Classification method

The EM algorithm starts with an initial segmentation with c classes and distribution parameter vector θ and works in an iterative manner. In each iteration, estimated parameters of current cluster are used to classify the image and the new segments are used to recompute the cluster parameters. Therefore it is necessary to consider the mixture model density function for the observation which can be formulated as:

$$f(C_i) = \sum_{r} p(C_i | r) \sum_{j} p(L_j = i | L_j, r \in \eta_r) f_j(C_i | \theta)$$  (1)

Where $p(L_j = i | L_j, r \in \eta_r)$ is prior probability for the class of pixel s, L, noted as I while the neighbouring pixels r in the neighbourhood $\eta_r$ are marked as $L_r$. Particularly the EM algorithm has three steps (Carson et al. 2002):

a. Initialization: Initializing the parameter $\theta$ of class $c$ according to the training samples. Initialization is one of the important steps of this approach because it has a certain impact on the final result. Poor initialization can converge in the local minima, and then the algorithm fails. Hence, we apply EM algorithm with three different initialization data. These initial data are random initialization, H/alpha classification maps and primary classification map which produced based on Mellin transform. In the next sections we will discuss them with details.

b. E-step: In this step, for each given observation, the posterior probabilities associated with the clusters are estimated using the current class-conditional PDF components and mixture proportions. For each pixel, the local MRF probability is calculated based on the classification result from the last iteration which updates all class parameters.

c. M-step: This step updates the distribution parameters for all the distribution models. For estimation of the texture parameters in the PolSAR distribution models, the method of matrix log-cumulant is applied (Anfinsen and Eltoft 2011). The EM algorithm sequentially repeats the E- and M-steps until the convergence point is met i.e. the percentage of pixels which are changing their classes is under a pre-set value.

2.2 Adaptive Markov Random Field

In the present paper, the method is proposed for PolSAR data classification by developing a Markovian energy function for the data statistics conditioned to each class, and an MRF model for the spatial context. To explore contextual information, MRF models are frequently used in many remote sensing applications. MRF assumes a local dependency for the spatial correlations. Under this assumption, the prior probability of a pixel s labelled as $L_s$ considering that its neighbouring pixel $r$ in the neighbourhood $\eta_r$ are marked as $L_r$ can be modelled with Gibbs law (Li 2009):

$$p(L_s = i | L_r, r \in \eta_r) = \frac{1}{Z_s} \exp\{-U(L_s | L_r, r \in \eta_r)\}$$  (2)

where $Z_s$ is a normalizing factor and $U$ denotes an energy function.

2.2.1 Adaptive neighbour structures: MRF theory enables the modeling of contextual dependencies between a set of sites. These sites might be pixels in an image or individuals in a social network. First and second-order neighbourhood systems are introduced as illustrated graphically in figure 2 and 3.

Figure 2. First-order neighbourhood system and its division into cliques. The black squares represent the site of interest and the white squares represent the neighboring sites.
is first order and (4) is second order moment of $\sum Z^L$.

By statistical analysis of product model we able to reach better formulation $T$ is texture and $W$ contain speckle characteristics. and positive definite Hermitian matrices. In this product model kind statistics of common radar distributions such as their transform and the simple expressions obtained for the Mellin transform is a natural analytical tool to study the distribution of the data more efficiently we used Mellin transform. Mellin kind statistics of common radar distributions such as their transform and the simple expressions obtained for the Mellin transform is a natural analytical tool to study the distribution of the data more efficiently we used Mellin transform. Mellin

$$K_3(Z) = \mu_3(Z) - \mu_1^3(Z)$$

$$K_5(Z) = \mu_5(Z) - 3\mu_3(Z)\mu_2(Z) + 2\mu_1^5(Z)$$

Where, $\mu_1$ is first order and $\mu_2$ is second order moment of product model $Z$ and the $v$-th order moment of product model are defined as (Anfinsen and Eltoft 2011):

$$\mu_v(Z) = \frac{1}{N} \sum_{i=1}^{N} (|n[Z_i]|^v)$$

3. RESULTS AND DISCUSSION

This unsupervised PolSAR classification starts with a preprocessing step for speckle reduction from data images. In the second step, the initialized values are obtained by three solution strategies (random, H/Alpha and Mellin transform). Then, the iteration procedure of E- and M-steps is performed. In the E-step pixel-wise model is combined with the MRF contextual model to take into account the spatial correlation between class labels. The classifier based on pixel statistics only, is severely affected by overlapping class statistics due to speckle noise. This problem is reduced by incorporating spatial contextual information. The EM algorithm is modified to include the contextual energy in the calculation of the posterior probabilities, and also, the spatial interaction parameter of the MRF model $\beta$ is estimated in the iteration process. The final classification map is obtained when the algorithm satisfy the statistical threshold.

The proposed algorithm has applied to a L-band PolSAR data sets, acquired by the UAVSAR over an agricultural area in Winnipeg, Canada. This area consists of a rich variety of annual crops including cereals, wheat, oilseeds, soybeans, corn, and pasture/forage. The images have been acquired in 5 July 2012 and are in multi look stokes matrix format. Figure 5 shows a 512x512 subsample of pauli decomposition which is used in this research.

$$U(L_i | L_r, r \in \eta_t) = -(\beta(1-b_r) \sum_{r=0}^{\eta_t} \delta(L_i - L_r))$$

Where $U$ is modified energy function and $\beta$ is a non-negative factor of the MRF model which quantifies the basic impact of the prior probability. For homogenous areas which $b_r$ limit to zero, the MRF analysis has greater impact in the labelling decision and a uniform class type is most likely to be present in this area. On the other hand, in heterogeneous area the MRF has less effect and various classes will be found.

2.3 Mellin transform

Analysis of the real PolSAR images shows that non-Gaussian models give a better representation of the data. Several distributions could be used to model PolSAR image texture with different spatial correlation properties and various degrees of inhomogeneity. For select optimum distribution which adapts the data more efficiently we used Mellin transform. Mellin transform is a natural analytical tool to study the distribution of products and quotients of independent random variables. The application of the Mellin transform to analysis of matrix-variate radar data builds on results in probability and the theory of statistical distributions. The separability induced by the Mellin transform and the simple expressions obtained for the Mellin kind statistics of common radar distributions such as their characteristic function, moments, cumulant and log-cumulant functions (Anfinsen and Eltoft 2011). If the product model of PolSAR data defined by $Z=TW$ which $Z$, $T$ and $W$ are complex and positive definite Hermitian matrices. In this product model formulation $T$ is texture and $W$ contain speckle characteristics. By statistical analysis of product model we able to reach better distribution function which have best fitting to our data in each classes. For this purpose for simplicity of computation we do it in Mellin kind matrix log-cumulants space. In this space several pixels with same distribution functions getting together and these log-cumulants will lead to more striking results. Second and third order log-cumulants functions defined as (Anfinsen and Eltoft 2011):

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To initialize the algorithm, first the image is randomly partitioned into a given number of segments. Figure 6 shows a random image used in this step.

Second method for initialization is based on H/alpha classification map. Entropy and alpha parameters of selected sub-sample are shown in figure 7.

Third strategy for initialization stage is a classification map generated based on Mellin transform. By separating different distribution functions of several classes based on Mellin transform we can reach a primary classification map. For this reason we present data in log-cumulant variable space. In this space, for each pixel the values of $K_2$ and $K_3$ are computed. This work helps to reach proper separation between several classes and distribution functions. Figure 8 illustrate log-cumulant diagram of used data.

This visual result show efficient performance of proposed approach for unsupervised PolSAR classification and boundaries of classes are detected properly. For the quantitative validation of presented approach 50 pixels are used to evaluate the confusion matrices, kappa coefficient and overall accuracy. These data have been uniformly selected from several classes. Table 1 shows quantitative comparison between the results of our approach with different initialization strategies and Wishart classification method.

| Method/ Accuracy | Sigma $^2$ | Kappa | Overall Accuracy (%) |
|------------------|-----------|-------|----------------------|
| Wishart method   | 3.87e-6   | 0.8721| 89.13                |
| Proposed Random  | 1.96e-6   | 0.8734| 89.49                |
| Proposed H/alpha | 8.34e-7   | 0.9269| 92.76                |
| Proposed Mellin  | 2.59e-7   | 0.9755| 98.02                |

Table 1. Quantitative comparison of the results.

In this table, overall accuracy and kappa coefficient show improvement of the proposed method by using Mellin transform for initialization stage. It is also clear even by random initialization the algorithm is able to reach acceptable results. Also the comparison of the Mellin-based initialized results with other well-known unsupervised algorithm is shown in figure 10.
4. CONCLUSION

In this paper a statistical approach is presented to unsupervised classification of PolSAR data images. This method by concerning contextual characteristics of PolSAR data, and using several strategies to initialize EM classification method leads to more reliable results. The importance of contextual analysis is revealed in the unsupervised classification using high resolution PolSAR data. Contextual analysis which is arrived by MRF has an important role for correct image modeling in classification. But the classical MRF’s energy function cannot involve relationship between pixels in PolSAR data in a neighboring system. For solving this problem, in this paper an adaptive energy function is presented which have a better contextual smoothing outcome. The quantitative comparison of the results emphasizes the efficiency of the proposed approach and the results demonstrate that developed unsupervised technique can be efficiently applied to PolSAR images from agricultural land and even urban area. The best results are achieved using Mellin-based initialization with contextual EM method and adaptive MRF. The proposed approach is able to produce homogenous mapping results with high accuracy and resulted classification map can be used in several applications of radar remote sensing.

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