It is not the parts, but how they interact that determines the behaviour of circadian rhythms across scales and organisms

Daniel DeWoskin, Weihua Geng, Adam R. Stinchcombe and Daniel B. Forger

Biological rhythms, generated by feedback loops containing interacting genes, proteins and/or cells, time physiological processes in many organisms. While many of the components of the systems that generate biological rhythms have been identified, much less is known about the details of their interactions. Using examples from the circadian (daily) clock in three organisms, Neurospora, Drosophila and mouse, we show, with mathematical models of varying complexity, how interactions among (i) promoter sites, (ii) proteins forming complexes, and (iii) cells can have a drastic effect on timekeeping. Inspired by the identification of many transcription factors, for example as involved in the Neurospora circadian clock, that can both activate and repress, we show how these multiple actions can cause complex oscillatory patterns in a transcription–translation feedback loop (TTFL). Inspired by the timekeeping complex formed by the NMO–PER–TIM–SGG complex that regulates the negative TTFL in the Drosophila circadian clock, we show how the mechanism of complex formation can determine the prevalence of oscillations in a TTFL. Finally, we note that most mathematical models of intracellular clocks model a single cell, but compare with experimental data from collections of cells. We find that refitting the most detailed model of the mammalian circadian clock, so that the coupling between cells matches experimental data, yields different dynamics and makes an interesting prediction that also matches experimental data: individual cells are bistable, and network coupling removes this bistability and causes the network to be more robust to external perturbations. Taken together, we propose that the interactions between components in biological timekeeping systems are carefully tuned towards proper function. We also show how timekeeping can be controlled by novel mechanisms at different levels of organization.

1. Introduction

Three levels of biochemical detail exist in the circadian timekeeping system of higher organisms, as well as many other rhythm generators: transcriptional regulation, post-translational modification and intercellular communication. For example, the mammalian daily (circadian) clock is controlled by the roughly 20,000 neurons of the suprachiasmatic nuclei (SCN), each of which has interlocked positive and negative genetic feedback loops in transcription and post-translational modifications that generate oscillations in the concentrations of core clock proteins with a period of 24 h. While many of the components of these timekeeping systems have been identified, how interactions between components at each of the three levels contribute to the generation of robust rhythms remains to be investigated. Here, we explore interactions at these three scales.

© 2014 The Authors. Published by the Royal Society under the terms of the Creative Commons Attribution License http://creativecommons.org/licenses/by/3.0/, which permits unrestricted use, provided the original author and source are credited.
1.1. Transcriptional regulatory elements

Genetic negative feedback loops lie at the core of many rhythmic processes within cells, including those involved in circadian timekeeping [1,2], embryogenesis [3], cell cycle [4] and DNA damage repair [5]. For example, at the core of the mammalian circadian clock is a negative feedback loop in which a transcriptional activating complex (BMAL::CLOCK) binds to E-boxes, transcriptional regulatory sites, in the promoters of the Per and Cry genes, activating their transcription. The protein products of these genes then form complexes, which return to the nucleus to bind to and deactivate BMAL::CLOCK, thereby inhibiting their own production. While multiple E-box DNA-binding sites for BMAL::CLOCK exist [6], little is known about their interaction.

A similar feedback loop structure exists in the circadian clocks of Drosophila and Neurospora [7,8]. One interesting twist is that the core repressor of the Neurospora clock, FRQ, also can stabilize activators, causing it to act as an activator as well [9]. Another Neurospora transcription factor involved in circadian timekeeping, VIVID, also acts as both an activator and repressor [10]. The bacterial transcription factor araC, used in a synthetic clock [11], can act as either a repressor or an activator at different sites [12]. Many other transcription factors show this property [13]. Thus, another possibility could be that a protein could act as both an activator and repressor by binding to different sites, which is a motif that remains to be explored in models of circadian clocks.

1.2. Protein complex formation

Following transcriptional regulation, many important phosphorylation and complex formation steps occur in cellular rhythm-generating systems [14,15]. They are difficult to model, as the number of possible complexes grows exponentially in the number of protein species that can bind. For example, in a recent detailed model of the mammalian circadian clock by Kim & Forger [16], the core negative feedback loop of the model focused on only six different proteins. However, the model had to account for almost 150 different possible species once all complexes were included, as well as nuclear transport and the action of kinases.

One specific example of complex formation in rhythm generation can be found in the Drosophila circadian clock. The expressions of four proteins, PERIOD (PER), TIMELESS (TIM), NEMO (NMO) and SHAGGY (SGG), are all under the control of a transcriptional complex, formed by the CLK and CYC proteins, that binds rhythmically to genes with E-boxes [17]. PER, TIM, NMO and SGG form a complex, where post-translational modifications occur, which control the rhythmic activation by CLK and CYC [18,19]. A similar complex is created in the mammalian and Neurospora circadian clocks. An outstanding question is whether the mechanism of protein complex formation matters in rhythm generation.

1.3. Coupled cellular networks

Finally, in addition to intracellular dynamics, intercellular signalling between cells also plays an important role in cellular rhythm-generating systems [20]. For example, isolated neurons of the SCN show weak, noisy rhythms [21] that can gain or lose rhythmicity in response to external stimuli [22]. When coupled together, however, these neurons form a robust circuit with precise 24 h oscillations that is resistant to genomic mutations [23]. Thus, important interactions on the network level lead to emergent behaviours that cannot be seen by considering only a single cell.

Here, we extend the Kim & Forger model [16] of intracellular dynamics to make a detailed multicellular model of the SCN. We explore how a multicellular SCN model is able to reproduce differences in phenotype between dispersed SCN neurons and the SCN network, which shows robust oscillations less affected by genomic mutations as well as external stimuli.

1.4. Overall goals

While our simulations have implications for specific rhythm-generating systems, especially circadian timekeeping in higher organisms, our results show that many important details of the biochemical mechanisms underlying rhythm generation in many systems remain unexplored. This may be because these simulations often require advanced computing techniques, such as the use of graphics processing units (GPUs) employed here, to simulate detailed multicellular biochemical models. While GPU computing is not the only method available for performing these simulations, it is particularly well suited for simulating networks of biological cells as the models are easily parallelizable on GPU cards and require sharing information between cells, which can be done rapidly using the globally available memory on a GPU card. With models at three different scales, we find that the interaction mechanisms used in circadian clocks favour robust oscillations.

2. Interactions between promoter-binding sites

Genetic networks require fine-tuning and control, generally provided in the form of transcriptional regulation. Even in a simple eukaryote such as yeast, as many as 37% of promoters were found to bind transcriptional regulators, and of these, more than one-third bound two or more regulators [24]. While these regulatory sites are now easily identified using high-throughput assays such as ChIPSeq [25], interactions between transcriptional regulators are much more difficult to characterize.

Here, we study transcriptional regulation in the context of a generalized feedback loop model based on that by Goodwin [26]. The model and corresponding equations are shown in box 1. We allow a general transcription rate, $f(P_i)$, which is a function of the concentration of a transcription factor $P_i$. We model two sites where $P_i$ can bind. In the first model, there are two repressive sites that act independently, as seen, for example in the E-boxes in the Per1 promoter [27]. It has previously been shown that complex behaviours, e.g. chaos, cannot be seen in such a simple system [28]. In the second model, two sites are again modelled, but one site acts to repress and one activates. Through this, we study how the interactions between transcriptional regulatory sites within a genetic feedback loop change oscillatory behaviour.

We searched for different types of oscillatory behaviour with different mechanisms of transcriptional regulation. To our surprise, we saw many types of behaviour, which had not yet been classified in genetic networks with just one feedback loop (although several had been seen in more complex networks [29,30]). One behaviour is called bistability, or hard excitation (figure 1a–c), where a stable steady state
Box 1. Description of a simple transcription–translation feedback loop model, with which we study the effects of transcriptional regulation mechanisms. A diagram of the feedback loop is shown, along with differential equations describing the dynamics of each of the protein species involved, and all parameters and initial conditions used.

![Feedback Loop Diagram](image)

The model equations take the form

$$\frac{dP_i}{dt} = f(P_i) - n_i P_i \quad \text{and} \quad \frac{dP_i}{dt} = m_i P_{i-1} - n_i P_i, \quad 2 \leq i \leq L.$$ 

This simple model of a biochemical feedback loop tracks the concentration of transcripts from a gene ($P_i$), and the concentration of protein translated from these transcripts. The protein can exist in several states ($P_2, \ldots, P_L$) due to post-translational modifications that eventually allow the protein to act as a transcription factor ($P_1$). The constant $n_i$ is the degradation rate of the transcript, and for $i > 1$, $n_i$ is the sum of the rate of translation of protein state $P_i$ and the conversion rate of protein state $P_i$ into the next state, $P_{i-1}$. Similarly, $m_i$ is the rate of translation of the protein, and $m_i$ (for $i > 2$) is the rate of conversion of protein $P_{i-1}$ into protein $P_i$. Here, we choose $L = 5$ and all rate constants to be 1. We also assume that there are two binding sites for $P_5$ on the gene. For simulations in figure 1c, the transcription rate (shown in figure 1a) was chosen to be

$$f(P_5) = \frac{aP^p}{P+p} + c \frac{bP^q}{bP+P},$$

where $a = 0.5$, $b = 0.75$, $c = 0.75$ and $p = 8$. In figure 1b, all initial conditions were chosen to be 0.5, and in figure 1c all initial conditions were chosen to be 0.7. In figure 1d–i, the transcriptional regulation function was of the form

$$f(P_5) = d + \left(\frac{cP^p}{aP+P}\right) \left(\frac{bP}{bP+P}\right).$$

For figure 1b, $p = 10$, $q = 25$, $a = 2$, $b = 0.2$ and $c = 9.25446$. In figure 1d, $d$ was chosen to be 0.055 and in figure 1h it was chosen to be 0.052826. These parameters were specifically chosen to show that a small change in parameters can yield a large change in behaviour. The initial conditions for figure 1e,h were that all variables started at values of 0.176. In figure 1c, $p = 10$, $q = 13$, $a = 1.0824$, $a = 0.423$, $b = 0.44$ and $d$ was chosen to be 0. The initial conditions for figure 1f,i were $P_1 = 0.07$, $P_2 = 0.4$, $P_3 = 0.8$, $P_4 = 0.2$ and $P_5 = 0.5$.

and a stable oscillatory state coexist [31]. The feedback loop displays either oscillations (figure 1b) or quiescence (figure 1c) depending on the initial conditions. In this model, oscillations can be started or stopped by external signals to the genetic network. This is a hallmark of many circadian clocks [29,32] and was found with the model of two repressive sites.

Allowing for interactions between an activator and repressor site greatly increases the behaviours that are possible. For example, during the course of an oscillation, the system spends near an equilibrium point. This additional equilibrium point could not be seen in the model of two repressive sites, because the transcription regulation function was monotonic.

Finally, we note that more complex behaviours including chaos, with sensitive dependence on initial conditions, can also be seen (figure 1g–i) with an activator and repressor sites. This is not possible in the model of two repressive sites [28]. These results show that it is not sufficient to simply know that a given transcription factor binds to a regulatory site on a gene. On the contrary, the mechanism of interaction between transcriptional regulatory sites can greatly influence the rhythmic behaviours created in a genetic feedback loop.

3. Interactions between proteins in complex formation

We next consider the mechanisms of post-translational modification, in particular complex formation. Inspired by the *Drosophila* circadian clock (see Introduction), we begin by considering a general system of $N$ distinct proteins (numbered 1 through $N$) that may combine to form complexes. Initially, the protein monomers are unbound, and we assume that proteins may not be repeated within a complex. We analyse the binding dynamics seen under three different models of complex formation:

- Model 1—individual proteins must bind one at a time to other individual proteins or existing complexes to create new complexes;
- Model 2—any individual protein or existing complex can bind to any other as long as no proteins are repeated within a complex; and
- Model 3—only proteins with consecutive indices can form a link in order to form a complex (i.e. 1 can only bind to 2, 2 can only bind to 1 or 3, 3 can only bind to 2 or 4, etc.).
Changes in transcriptional regulation can drastically affect the behaviour of genetic oscillators. We consider three possible mechanisms of transcriptional regulation, where the rate of transcription as a function of a transcription factor is plotted in (a), (d) and (g) (box 1). Each assumes that there are two regions on a promoter where a transcription factor ($P_i$) can bind. In the first model (shown in (a)), binding to either site can stop transcription. For this mechanism, the system can either show oscillations (b) or quiescence (c) depending on the initial state of the system. In models (d) and (g), binding at one site activates transcription and binding at the other site represses transcription. For model (d), small changes in the transcription regulation function can change the shape of oscillations and can lengthen the period (e–f). With a different choice of transcriptional regulation function, shown in (g), chaotic behaviour can also be seen (h–i). Rate constants and initial conditions can be found in box 1. For each simulation, an initial transient is not shown.

These three models are depicted in figure 2 for the case $N = 4$, which we will use as an illustrative example because our motivating problem in Drosophila contains four proteins. Beginning with the four unbound proteins, figure 2 shows the sequence of reactions needed in order to make all possible complexes allowed under each binding model. Models 1 and 2 lead to the formation of the same intermediate complexes before a full complex containing all four subunits is formed, but they are formed through different reactions. For example, in Model 2, heterodimer 12 may bind with 34 to form the full complex 1234. Such a reaction is not permissible under Model 1. With Model 3, some complexes cannot form, for example the heterodimers 13, 14 and 24 are never produced. Table 1 summarizes all of the complexes that may be formed for the three models.

For each model, we consider initial concentrations of 1 for each of the four proteins and set all rate constants to 1. All reactions are assumed to occur by standard mass action kinetics. We initially consider only complex formation reactions and do not model transcription, translation or degradation of any of the protein monomers. Thus, no new monomers will be formed, and monomers are lost only to complex formation. Figure 3a shows the accumulation of the tetramer 1234 over time under each of the three models. Only in Model 3 does the concentration of the tetramer approach a value near 1, indicating that nearly all the individual proteins eventually participate in the formation of this complex. In the other models, most of the individual proteins are locked up in intermediate complexes that are unable to bind together. This is depicted in figure 3b, which shows the steady-state distribution of the protein complexes formed under each of the three models. Models 1 and 2 result in many intermediate complexes that are unable to bind to one another. Under Model 3, on the other hand, almost all monomers are bound in a tetramer.

This simple example illustrates that the mechanism of protein binding strongly affects the distribution and dynamics of complex formation. To apply this principle to study biological rhythms generated by a transcription–translation feedback loop (TTFL), we consider the case that the full tetramer (1234) negatively feeds back on the production of the four monomers, which are also linearly degraded. This leads to differential equations of the form

$$\frac{dM_i}{dt} = \frac{1}{1 + (P_{1234}/K_M)^n} - M_i, \quad i = 1, \ldots, 4$$

and

$$\frac{dP_i}{dt} = M_i - \nu P_i - \gamma (P_{1}, \ldots, P_{1234}), \quad i = 1, \ldots, 4,$$

where $M_i$ and $P_i$ are the concentrations of mRNA and protein for monomer $i$, and $\nu$ is the protein degradation rate. The functions $\gamma_i$ describe the mass action binding reactions between $P_i$ and the other species, and differ for the three models of
complex formation described previously. We assume that degradation and translation of the transcripts for each protein occur with rate 1. Transcription occurs according to a standard Hill function with Hill coefficient \( n \) and repression constant \( K_r \).

As before, complexes are gained and lost through binding events, but now in addition, they undergo linear degradation with rate constant \( v \). We assume saturating degradation for the final tetramer, leading to a differential equation of the form

\[
\frac{dP_{1234}}{dt} = f_{1234}(P_1, \ldots, P_{1234}) - \frac{v_{1234}P_{1234}}{K_m + P_{1234}}
\]

where \( f_{1234} \) describes the binding reactions which form \( P_{1234} \), and \( v_{1234} \) and \( K_m \) are the maximal degradation rate and associated Michaelis–Menten constant, respectively. Our motivation for this is to create a stable final complex, at least for higher concentrations, which is in agreement with the available biochemical data [33].

After searching the parameter space, we were able to obtain oscillations in each of the models. We plot the concentration of protein 1 for all three models in figure 4(a) and the concentration of the final tetrameric complex in figure 4(b) for a nominal choice of parameters for which all three models oscillate. The value of the Hill coefficient determines whether oscillations are seen, and their frequency and amplitude. To study this, we show a bifurcation diagram in \( n \) in figure 4(c). Oscillations occur as the Hill coefficient is increased. The value of \( n \) for which oscillations first occur is smallest for Model 3, then Model 2 and finally Model 1. This nesting of the oscillatory region also occurs for the \( K_m \) parameter. In figure 4(d), we show a bifurcation diagram in \( K_m \), which controls the location of the onset of saturating degradation of the tetramer. All three models oscillate for small \( K_m \) and are non-oscillatory for large \( K_m \). For intermediate \( K_m \) (so that the mean value of the tetramer is near \( K_m \), Models 1, 2 and 3 do not oscillate, oscillate with small amplitude and strongly oscillate, respectively. The nesting of the oscillatory regions for the three models holds true for other choices of nominal

---

**Table 1.** Complete list of all protein complexes formed for the case \( N = 4 \) in the three models. Models 1 and 2 lead to the formation of the same complexes, but not all of these complexes can be formed in Model 3. (Online version in colour.)

| no. | Models 1 and 2 | Model 3 |
|-----|----------------|---------|
| 1   | 1              | 1       |
| 2   | 2              | 2       |
| 3   | 3              | 3       |
| 4   | 4              | 4       |
| 5   | 1 2            | 1 2     |
| 6   | 1 3            | 2 3     |
| 7   | 1 4            | 3 4     |
| 8   | 2 3            | 1 2 3   |
| 9   | 2 4            | 2 3 4   |
| 10  | 3 4            | 1 2 3 4 |
| 11  | 1 2 3          |         |
| 12  | 1 2 4          |         |
| 13  | 1 3 4          |         |
| 14  | 2 3 4          |         |
| 15  | 1 2 3 4        |         |

---

**Figure 2.** Three generic models of complex formation. Here, we consider four proteins, which can bind by several mechanisms of complex formation. In (a), we assume that any protein complex can bind only with individual proteins that are not part of the complex. In (b), we assume that any complex can bind with any other complex so long as they do not both contain any common individual proteins. In (c), we assume that only proteins with consecutive indices can form a link in order to form a complex. The left most panel indicates the isolated proteins. The next panels show the possible complexes that can form after one, two or three reactions, respectively. Complexes with one, two, three or four proteins are represented as circles of increasing sizes (coloured blue, orange, green and red, respectively, in the online version). (Online version in colour.)
parameters as can in part be seen from the $K_m - n$ two-parameter bifurcation diagram in the electronic supplementary material, figure S1.

Together, these results show that the mechanism of repressor complex formation in a negative feedback loop strongly affects whether or not rhythms are generated. Moreover, we find that Model 3 (which seems the most likely candidate used in the Drosophila circadian clock) has the most likely chance of yielding oscillations.

4. Interactions between cells in a network

We next study how interactions between cells within the SCN, the central mammalian circadian pacemaker, can determine the behaviour of the tissue. Previous studies of the circadian timekeeping system have shown that coupling between cells can help heterogeneous neurons with weak, damped oscillations [35,36] or only stochastic oscillations [37] to generate rhythms as a synchronized network. Coupling has also been shown to affect the ability of the network to entrain to external stimuli [38]. Indeed, several previous models of the SCN have been built [2,16,35,36,39–46], but generally many of the details of transcriptional and post-translational regulation are left out. Additionally, the role of coupling between cells in the model is important for fitting parameters, which is often not considered.

Models of individual cells are routinely fitted to data from populations. Here, we develop a detailed biochemical model of the SCN, fit parameters that incorporate intercellular coupling to population data, and then compare the result to the same model when coupling is removed. Our goal is to use the model to understand how intercellular signalling leads to emergent phenomena at the network level.

We aim to match experimental measurements of the SCN from both the dispersed cell culture (uncoupled neurons) and organotypic slice preparations (coupled neurons). SCN slices contain a two-dimensional array of neurons, each of which could generate timekeeping. To represent the intracellular rhythms, we use the Kim & Forger model [16] for the mammalian circadian clock, which includes detailed descriptions of complex formation, and transcriptional regulation by the repressor complexes formed. We chose the Kim and Forger model because of its detail and predictive accuracy.

4.1. Suprachiasmatic nuclei model formulation

We first extend the Kim and Forger model of intracellular rhythms in the SCN to a tissue-level SCN model by incorporating intercellular signalling. In particular, we focus on the effects of the neuropeptide vasoactive intestinal peptide (VIP), which has been reported to be the most essential signalling molecule in the SCN [20,47–51]. VIP is released by roughly 20% of the
neurons of the SCN and received by the cell-surface VPAC$_2$ receptor (VPAC$_2$R). This receptor has been shown to be present on the surface of upwards of 90%, if not all cells in the SCN [52], so we will assume all cells can receive VIP. Reports about whether VIP is produced rhythmically or not conflict [53–55], but it is generally agreed upon that VIP release should be rhythmic [56], so we focus only on VIP release.

Binding of VIP to the receptor initiates an intracellular signalling cascade with several steps occurring on a very fast time scale (figure 5). Condensing this fast time scale, we model only the ligand–receptor binding and a few key steps in the pathway for which we have experimental data to compare. Specifically, we assume that VIP binding to the receptor leads to an increase in cAMP, which promotes phosphorylation and activation of cyclic AMP response element binding protein (CREB). The activated CREB then binds to the cyclic AMP response element (CRE) sites on the promoters of the Per1 and Per2 genes, increasing their transcription [57].

The rate of VIP release is assumed to be proportional to intracellular calcium levels, and calcium can also, through a parallel pathway, promote the phosphorylation of CREB directly [58]. In intracellular calcium is assumed to increase at a rate proportional to E-box activity and decrease at a linear rate. While this is a purely phenomenological assumption, it is consistent with experimentally measured time courses of intracellular calcium, which show the greatest increase roughly

Figure 4. Different oscillatory regions in parameter space are observed under the three models of complex formation when placed in a TTFL. Sample trajectories for (a) the first monomer, 1, and (b) the final tetrameric complex, 1234, are shown for all three models ($n = 5$, $y = 0.4$, $K_l = 0.004$, $K_m = 0.4$, $v_{1234} = 0.05$). (c) A bifurcation diagram in $n$ showing that with a sufficiently high Hill coefficient, oscillations occur in each of the models. (d) A bifurcation diagram in $K_m$ showing that the pattern of onset and offset of oscillations as $K_m$ is reduced varies between the three models. In the bifurcation diagrams, computed using XPPAUT v. 7.0 [34], a solid line denotes a stable equilibrium or limit cycle and a dashed line represents an unstable equilibrium.

![Diagram of steps of CRE activation pathway](image)

Figure 5. Diagram of the steps of the CRE activation pathway included in the model. Binding of VIP to the cell-surface receptor VPAC$_2$R leads to increases in cAMP, which together with intracellular calcium promote the phosphorylation and activation of CREB. CRY non-competitively binds the intracellular domain of VPAC$_2$R, inhibiting it. Activated CREB binds to CRE sites on the promoters of the Per1 and Per2 genes increasing their transcription. at the time of maximal E-box activity [59,60], and creates a phase difference between calcium and the molecular clock components consistent with those found experimentally as well as in previous modelling studies [43]. Finally, CRY1 and
CRY2 are assumed to inhibit the adenylyl cyclase activity of VPAC₂R [61]. This pathway is diagrammed in figure 5, and all equations, variables, and parameters modified from the original Kim and Forger model, or added to make this new model are given in the electronic supplementary material, S2.

4.2. Parameter estimation and simulating the suprachiasmatic nuclei model with graphics processing units

The addition of intercellular signalling to the Kim and Forger model requires the fitting of 15 new parameters. To represent a single cell, Per1 and Per2 maximal E-box transcription rates (parameters trPo and trPt) were set to 40% of their originally published maximal values, as recommended in the original manuscript, and all other original parameters were unchanged [16]. This was done to allow for additional Per transcription initiated by CRE activation through VIP and calcium. The 15 new parameters were fitted using simulated annealing as in the original Kim and Forger publication [16]. In addition to the protein and mRNA time courses and protein abundance data that the original model was fitted to, we additionally fit to time courses of intracellular calcium and CRE activity levels, extracted from published videos [59] using MATLAB. To fit parameters for a single cell in the SCN network, we coupled the cell to itself so that it received the VIP that it produced. This allowed us to fit the activation of the CRE pathway by VIP in a single cell. For simulation of the whole SCN, the VIP released by each cell was divided by the number of VIP-producing cells, so that the input signal from the network was of the order of the originally fitted VIP level. Further details on the methods of parameter estimation are given in the electronic supplementary material, S3.1. Fits of the model to experimental data obtained are shown in figure 6.

We simulate an SCN network model of 1024 cells in total and assume that VIP is produced by 205 of the cells (approx. 20%). VIP is a small neuropeptide, which should diffuse rapidly throughout the SCN compared with the time scale of transcriptional activation. Therefore, we make the simplifying assumption that the VIP-producing cells released VIP equally to all cells in the SCN. For simulation of the whole SCN, the VIP released by each cell was divided by the number of VIP-producing cells, so that the input signal from the network was of the order of the originally fitted VIP level. Further details on the methods of parameter estimation are given in the electronic supplementary material, S3.1. Fits of the model to experimental data obtained are shown in figure 6.

Figure 6. Fits of the extended single-cell model to mRNA, protein, CRE activity and Ca²⁺ time series. Model predictions are shown as smooth curves, and experimental data as squares. All time series are normalized by their maximum values. mRNA and protein time series are the same as used in [16]. CRE and Ca²⁺ time series extracted from videos in [59].
Heterogeneity is included in the model by allowing the Per1 and Per2 maximal transcription rates associated with both E-box activation (parameters trPo and trPt, respectively) and CRE activation (parameters CtrPo and CtrPt, respectively) to vary between cells. For each cell, these four parameters were drawn independently from normal distributions with mean equal to the value from our fitted single-cell model, and standard deviation 5% of the mean. This affects the strength of oscillations seen in individual cells as well as their intrinsic periods of oscillation. Only these transcription rates were varied between cells; all other parameters were set to the values fitted as described above.

Both the parameter estimation algorithm and simulation of the network model are accelerated using GPU computing. This architecture is well suited for these problems because of their structure. Parameter estimation using simulated annealing is embarrassingly parallel and fits entirely within the memory onboard the GPU card. Simulation of the SCN network is also sufficiently small to fit in memory; however it does require some communication between threads. In particular, information about intercellular coupling through VIP must be passed between cells, but this is a small amount of data relative to the computation of the intracellular dynamics, which can be solved in independent blocks. For our problem, we choose to simulate 1024 cells in parallel, either uncoupled for parameter estimation, or coupled for the SCN network model, because tests showed that this was a near optimal choice in terms of speed of computation per number of cells (see the electronic supplementary material, figure S2). Details of the computational methods used are given in the electronic supplementary material, S3.

4.3. Differences between single cell and whole suprachiasmatic nuclei behaviour

We consider our model both in the presence and absence of coupling through VIP. Raster plots of PER2 levels for 200 randomly selected cells (out of 1024) from the coupled SCN model are shown in figure 7a. Cells within the intact SCN have well-synchronized, high-amplitude rhythms. The uncoupled model mimics the dispersed cell preparations often used experimentally. In these simulations, the VIP release rate (parameter vpr) is set to zero, as cells are assumed to be dispersed enough that they are unable to signal through VIP release. Raster plots of PER2 levels for the uncoupled model are shown in figure 7b. In the absence of coupling, the cells desynchronize and show a drastic reduction in rhythm amplitude, with some losing rhythmicity altogether. While the uncoupled cells all begin with similar initial conditions, they drift apart over time due to their differences in intrinsic periods. Periods of individual cells range from 24.0 to 25.6 with a mean of 24.79 ± 0.29 and are distributed roughly normally. Of the 1024 isolated cells simulated, 966 showed sustained rhythms while the other 58 were arrhythmic or heavily damped.

Consistent with the original model [16], we find that our uncoupled model matches known single-cell genotypic knockouts: 70% of Per1−/− and all Cry1−/− cells modelled were arrhythmic, while Cry2−/− cells were mostly rhythmic (918 of 966 rhythmic) with a long period (mean 27.13 ± 0.38 h). This is all consistent with experimental data for SCN neurons in dispersed culture [23]. In the coupled SCN model with intact VIP signalling, cells synchronize with a period of 24.2 h, consistent with SCN explants [23]. Unlike the isolated cells, the network model is resistant to genotypic knockouts, showing robust rhythms in Per1−/−, Cry1−/− and Cry2−/− individual knockouts, with no period change, period shortening by approx. 1 h, and period lengthening by approx. 1.5 h, respectively, for the three knockouts.

To test the robustness of individual cellular rhythms, we constructed a phase response curve (PRC) to VIP to see how they phase change in response to external signalling. For this curve, circadian time was determined relative to the cell’s PER2 protein level, with the peak PER2 level defined as CT12. Individual cells can show both large phase advances as well as delays depending on the time at which the VIP is applied, and surprisingly can also be made arrhythmic (denoted as a gap in the PRC). A PRC for a single cell is shown in figure 8a. For this particular cell, a VIP pulse between CT17.3 and CT20.5 causes the cell’s rhythms to damp (figure 8c), in stark contrast to the quickly recovered rhythms when the pulse is given at other circadian times (figure 8d). This bistability was surprising, as it had not been seen with the parameters used in the original Kim and Forger model, and is a novel prediction of our new single-cell model. It is, however, consistent with experiments which have shown that application of forskolin, a direct stimulant of the cAMP signalling pathway, to isolated SCN neurons can cause the cells to gain or lose rhythmicity [22]. Other models have also found this behaviour, notably in the light response of the Drosophila circadian clock [29] and in a particular range of parameters in an overall model of mammalian circadian rhythms [62].

In our model, bistability is a property of the individual cellular oscillators, but not of the SCN network. VIP pulses of identical magnitudes applied to the SCN network show...
much smaller phase shifts, with a traditional type I PRC, as described in [32], shown in figure 8b (note the difference in scale). Thus, the intercellular coupling confers robustness against external perturbations. The SCN network PRC qualitatively matches that found experimentally [47], with roughly the same pattern of advances and delays. The main notable difference is that the magnitude of the phase delays is not as great as in [47], which could be explained by the pharmacokinetics of VIP, or small differences in the magnitude of the VIP pulse given, as compared to our simulations.

To explore this bistability in single cells further, we tested whether the reintroduction of VIP signalling could restart collective rhythms in the network. Using our uncoupled model from before, we began with half the cells in the rhythmic state and the other half in the arrhythmic state, and reintroduced VIP signalling. Plots of 32 representative cells from the 1024 in the network with varying initial amplitudes (with bright to dark colours representing low to high initial amplitudes, respectively) and phases are shown in figure 8e. After restoring VIP signalling (time denoted by the red vertical line), all of the cells in the network quickly regained high-amplitude rhythms and resynchronized over time. This illustrates the fact that bistability is not seen in the coupled network, but is seen in isolated cells.

5. Discussion
Here, we have shown that the details of how parts of a rhythm-generating system interact play a crucial role in determining the behaviour of biological clocks. These details are often not included in the summary diagrams biologists use
to describe biochemical interactions. Our results demonstrate that they are crucially important at every step of rhythm generation in a genetic network; from transcriptional regulation, to post-translational modification, and finally to intercellular communication. We also show that much more investigation may be needed to determine the parts of timekeeping networks that are crucial for behaviour.

Combinatorial complexity is seen in many biological systems. This is because almost all cellular processes involve protein complex formation. It is thus surprising that so few studies have included the details of protein complex formation. We find that they can be crucial in correctly predicting a system’s behaviour. Many of the behaviours we have described such as chaos and bistability have been seen in more complex models of biological timekeeping [63–65]. By studying a simple negative feedback loop, we show how they can be attributed to the way in which transcriptional regulators interact, an often overlooked but essential step in rhythm generation.

The development of detailed multicellular models of biological tissues has the potential to explore many complicated phenomena seen experimentally, and to try to explain the mechanisms behind them. An important area for future work is to study the differences in phase among neurons in the SCN network. Heterogeneity of period and phase within the SCN has been shown to be important for the coding of seasonal changes in light and dark cycles [66–68]. Previous studies have shown that cells in subregions of the SCN exhibit differences in intrinsic period [66,69–71], and some have suggested that these period differences drive the spatio-temporal pattern or ‘phase wave’ seen in SCN slices [71].

With our SCN model, we focused on the molecular mechanisms of rhythm generation. In the actual SCN, there is a strong connection between the molecular clock and the electrical activity of the cells [72], and previous studies have shown that the rhythms in electrophysiology can strengthen molecular rhythms [43]. While we have not considered this aspect of rhythm generation here, we plan to explore it in future work.

Here, we show how coupling can make the SCN more resistant to perturbations, which is in agreement with experimental findings [73]. Our findings also show how coupling greatly increases the amplitude of rhythms, which also matches experimental findings [20,74]. But most interestingly, we find that when cellular coupling is included in model fitting, individual cells lacking the coupling signal become bistable. This matches data which show that timekeeping in individual isolated neurons within the SCN can be turned on or off by biochemical signals. It also raises questions about our single-cell simulations of circadian mutants and the data that we compare our simulations against [23]. When single cells are arrhythmic, it remains to be seen if that is due to bistability or if the cells are incapable of rhythmicity. This needs to be explored both in simulations and in the experimental preparation.

The designs we have tested are inspired by the experimental findings from the circadian clock found in several organisms. While more work is needed, our findings point towards circadian clocks using mechanisms that yield robust oscillations. The results presented here are numerical, and further mathematical analysis could expand these results [75]. The core negative feedback loop that generates timekeeping in many organisms is controlled by one or multiple E-boxes, which are repressed by elements in the feedback loop. We find this design can yield bistability, but not chaos. Additionally, we find that bistability in intracellular timekeeping, which makes timekeeping vulnerable to perturbations, can be compensated for by intercellular coupling.

Further experimental work is needed to verify our predictions. It would be interesting to build a synthetic clock where a protein, under negative feedback, acts both as an activator and repressor. Such a design could show behaviours not yet seen in synthetic clocks, especially as the araC protein, which can show this behaviour, has already been included in a synthetic clock. We also predict that individual isolated SCN neurons are bistable. This matches data presented in Webb et al. [22], but better experimental data would characterize the single-cell PRC to VIP and the possibility that it could stop rhythmicity, offering experimental validation of our prediction. We also note that the protein binding scheme that is most likely to show oscillations matches what is currently known about NMO, PER, TIM and SGG, at least that NMO binds PER, PER binds TIM and TIM binds SGG [18,19]. However, the interactions between these four proteins are not yet fully worked out, which could be validated by a two-hybrid system followed by a detailed biochemical study. While the details of these interactions could be difficult to determine, our results indicate that their importance makes this effort worthwhile.

Acknowledgements. We would like to thank Jihwan Myung for helpful discussions and graphical design, as well as Seth Meyer for technical support and assistance with GPU computing.

Funding statement. This work was supported by a programme grant from the Human Frontiers of Science Programme (RPG 24/2012) and a grant from the Biomathematics Programme at the Army Research Laboratory W911NF-13-1-0449.

References

1. Ko CH, Takahashi JS. 2006 Molecular components of the mammalian circadian clock. Hum. Mol. Genet. 15, R271–R277.
2. Forger DB, Peskin CS. 2003 A detailed predictive model of the mammalian circadian clock. Proc. Natl Acad. Sci. USA 100, 14,806 – 14,811. (doi:10.1073/pnas.203628100)
3. Schrider C et al. 2010 Topology and dynamics of the zebrafish segmentation clock core circuit. PLoS Biol. 10, e1001364. (doi:10.1371/journal.pbio.1001364)
4. Chen KC, Calzone L, Csikasz-Nagy A, Cross FR, Novak B, Tyson JJ. 2004 Integrative analysis of cell cycle control in budding yeast. Mol. Biol. Cell 15, 3841 – 3862. (doi:10.1091/mbc.E03-11-0794)
5. Lev Bar-Or R, Maya R, Segel LA, Alon U, Levine AI, Oren M. 2000 Generation of oscillations by the p53-Mdm2 feedback loop: a theoretical and experimental study. Proc. Natl Acad. Sci. USA 97, 11,250 – 11,255. (doi:10.1073/pnas.210171597)
6. Le Martelot G et al. 2012 Genome-wide RNA polymerase II profiles and RNA accumulation reveal kinetics of transcription and associated epigenetic changes during diurnal cycles. PLoS Biol. 10, e1001442. (doi:10.1371/journal.pbio.1001442)
7. Williams JA, Sehgal A. 2001 Molecular components of the circadian system in Drosophila. Annu. Rev. Physiol. 63, 729 – 755. (doi:10.1146/annurev.physiol.63.1.729)
18. Gallego M, Virshup DM. 2007 Post-translational phosphorylation-dependent maturation of Neurospora circadian clock protein from a nuclear repressor toward a cytoplasmic activator. Genes Dev. 20, 297–306. (doi:10.1101/gad.360906)

19. Gin E, Diemeliller ACR, Brunner M, Hofer T. 2013 The Neurospora photoreceptor VIVID exerts negative and positive control on light sensing to achieve adaptation. Mol. Syst. Biol. 9, 667. (doi:10.1038/msb.2013.24)

20. Stricker J, Cookson S, Bennett MR, Mather WH, Tsimring LS, Hasty J. 2008 A fast, robust and tunable synthetic gene oscillator. Nature 456, 516–519. (doi:10.1038/nature07389)

21. Meeker K, Harang R, Webb AB, Welsh DK, Doyle FJ, Bonnet G, Herzog ED, Peitzold LR. 2011 Wavelet measurement suggests cause of period instability in mammalian circadian neurons. J. Biol. Rhythms 26, 353 – 362. (doi:10.1177/0747730411409663)

22. Webb AB, Angelo N, Huettner JE, Herzog ED. 2009 Intrinsinc, nondeterministic circadian rhythm generation in identified mammalian neurons. Proc. Natl Acad. Sci. USA 106, 16 493 – 16 498. (doi:10. 1073/pnas.0902768106)

23. Liu AC et al. 2007 Intercellular coupling confers robustness against mutations in the SCN circadian clock network. Cell 129, 605 – 616. (doi:10.1016/j.cell.2007.02.047)

24. Lee T et al. 2002 Transcriptional regulatory networks in Saccharomyces cerevisiae. Science 298, 799 – 804. (doi:10.1126/science.1075090)

25. Johnson DS, Mortazavi A, Myers RM, Wold B. 2007 Genome-wide mapping of in vivo protein-DNA interactions. Science 316, 1497 – 1502. (doi:10.1126/science.1143139)

26. Goodwin B. 1966 An entrainment model for timed enzyme syntheses in bacteria. Nature 209, 479 – 481. (doi:10.1038/209479a0)

27. Froy O, Chang DC, Reppert SM. 2002 Redox potential: differential roles in dCRY and mCRY functions. Curr. Biol. 12, 147 – 152. (doi:10.1016/S0960-9822(01)00566-X)

28. Mallet-Paret J, Smith HL. 1990 The Poincare–Bendixon theorem for monotone cyclic feedback systems. J. Dyn. Differ. Equ. 2, 367 – 421. (doi:10.1007/BF01054041)

29. Leloup JC, Goldbeter A. 2001 A molecular explanation for the long-term suppression of circadian rhythms by a single light pulse. Am. J. Physiol. Regul. Integr. Comp. Physiol. 280, R1206 – R1212.

30. Guantes R, Yoyatos JF. 2006 Dynamical principles of two-component genetic oscillators. PLoS Comput. Biol. 2, e30. (doi:10.1371/journal.pcbi.0020030)

31. Forger DB, Paydarfar D. 2004 Starting, stopping, and resetting biological oscillators: in search of optimal perturbations. J. Theor. Biol. 230, 521 – 532. (doi:10.1016/j.jtbi.2004.04.043)

32. Winfree AT. 2002 The geometry of biological time. New York, NY: Springer.

33. Vosshall LB, Price JL, Sehgal A, Saez L, Young MW. 2002 Transcriptional regulatory networks control circadian phase resetting in Drosophila. Genes Dev. 16, 2374 – 2386. (doi:10.1101/gad.360906)

34. Abreu MS, Zadina A, Luo W, Tkachev S, Rosbash M. 2011 CLOCK target gene characterization: from a nuclear repressor toward a cytoplasmic activator. Philos. Trans. R. Soc. B 366, 3792 – 3803. (doi:10.1098/rstb.2010.0490)

35. Ko CH et al. 2010 Emergence of noise-induced oscillations in the central circadian pacemaker. PLoS Biol. 8, e1000513. (doi:10.1371/journal.pbio.1000513)

36. Abraham U, Granada AE, Westermark PO, Heine M, Piggins HD, Cutler DJ, 2003 The roles of vasoactive intestinal polypeptide in the mammalian circadian clock. J. Endocrinol. 177, 7 – 15. (doi:10.1677/joe.0.170007)

37. Vosshall LB, Price JL, Sehgal A, Saez L, Young MW. 2002 Transcriptional regulatory networks control circadian phase resetting in Drosophila. Genes Dev. 16, 2374 – 2386. (doi:10.1101/gad.360906)

38. Abraham U, Granada AE, Westermark PO, Heine M, Kramer A, Herzog H. 2010 Coupling genes to entrainment range of circadian clocks. Mol. Syst. Biol. 6, 438. (doi:10.1038/msb.2010.92)

39. Minsky HP, Liu AC, Welsh DK, Kay SA, Doyle FJ. 2009 A model of the cell-autonomous mammalian circadian clock. Proc. Natl Acad. Sci. USA 106, 11 107 – 11 112. (doi:10.1073/pnas.0909483106)

40. Gonze D, Bernard S, Waltermann C, Kramer A, Herzog H. 2005 Spontaneous synchronization of coupled circadian oscillators. Biophys. J. 89, 120 – 129. (doi:10.1529/biophysj.104.058388)

41. Becker-Weimann S, Wolf J, Herzog H, Kramer A. 2004 Modeling feedback loops of the mammalian circadian oscillator. Biophys. J. 87, 3023 – 3034. (doi:10.1529/biophysj.104.049824)

42. Religio A, Westmark PD, Wallach T, Schellenberg K, Kramer A, Herzog H. 2011 Tuning the mammalian circadian clock: robust synergy of two loops. PLoS Comput. Biol. 7, e1002309. (doi:10.1371/journal.pcbi.1002309)

43. Diekmann CO, Belle MDC, Irwin RP, Allen CN, Piggins HD, Forger DB. 2013 Causes and consequences of hyperexcitation in central clock neurons. PLoS Comput. Biol. 9, e1003196. (doi:10.1371/journal.pcbi.1003196)

44. Leloup JC, Goldbeter A. 2003 Toward a detailed computational model for the mammalian circadian clock. Proc. Natl Acad. Sci. USA 100, 7051 – 7056. (doi:10.1073/pnas.1132112100)

45. Vasalou C, Henson MA. 2010 A multiscale model to investigate circadian rhythmicity of pacemaker neurons in the suprachiasmatic nucleus. PLoS Comput. Biol. 6, e1000706. (doi:10.1371/journal.pcbi.1000706)

46. Vasalou C, Henson MA. 2011 A multicellular model for differential regulation of circadian signals in the core and shell regions of the suprachiasmatic nucleus. J. Theor. Biol. 288, 44 – 56. (doi:10.1016/j.jtbi.2011.08.010)

47. An S, Irwin RP, Allen CN, Tsai C, Herzog ED. 2011 Vasoactive intestinal polypeptide requires parallel changes in adenylyl cyclase and phospholipase C to entrain circadian rhythms to a predictable phase. J. Neurophysiol. 105, 2289 – 2296. (doi:10.1152/jn.00966.2010)

48. Aton SJ, Colwell CS, Harmar AJ, Waschek JA, Piggins HD. 2005 Vasoactive intestinal polypeptide mediates circadian rhythmicity and synchrony in mammalian clock neurons. Nat. Neurosci. 8, 476 – 483. (doi:10.1038/nn1419)

49. Harmar AJ. 2003 An essential role for peptidergic signalling in the control of circadian rhythms in the suprachiasmatic nucleus. J. Neuroendocrinol. 15, 333 – 338. (doi:10.1046/j.1365-2826.2003.00105.x)

50. Brown TM, Colwell CS, Waschek JA, Piggins HD. 2007 Disrupted neuronal activity rhythms in the suprachiasmatic nucleus of vasoactive intestinal polypeptide-deficient mice. J. Neurophysiol. 97, 2553 – 2558. (doi:10.1152/jn.01206.2006)

51. Piggins HD, Gutler DJ. 2003 The roles of vasoactive intestinal polypeptide in the mammalian circadian clock. J. Endocrinol. 177, 7 – 15. (doi:10.1677/joe.0.170007)
52. An S, Tsai C, Ronecker J, Bayly A, Herzog ED. 2012 Spatiotemporal distribution of vasoactive intestinal polypeptide receptor 2 in mouse suprachiasmatic nuclei. J. Comp. Neurol. 520, 2730 – 2741. (doi:10.1002/cne.23078)

53. Yang J, Cagampang FR, Nakayama Y, Inouye SI. 1999 Circadian rhythms of neuropeptides in the suprachiasmatic nucleus. Prog. Brain Res. 111, 75 – 90. (doi:10.1016/S0079-6123(08)60401-X)

54. Inouye ST. 1996 Circadian rhythms of neuropeptides in the suprachiasmatic nucleus. Brain Res. Mol. Brain Res. 20, 259 – 262. (doi:10.1016/0169-328X(93)90049-U)

55. Shinohara K, Honma S, Katsuno Y, Abe H, Honma K. 1991 Daily variations in concentration of vasoactive intestinal polypeptide immunoreactivity in discrete brain areas of the rat. Brain Res. 538, 136 – 140. (doi:10.1016/0006-8993(91)90387-B)

56. Shinkawa K, Honma S, Katsumo Y, Abe H, Honma K. 1994 Circadian rhythms in the release of vasoactive intestinal polypeptide and arginine–vasopressin in organotypic slice culture of rat suprachiasmatic nucleus. Neurosci. Lett. 170, 183 – 186. (doi:10.1016/0304-3940(94)90269-0)

57. Travnickova-Bendova Z, Cermakian N, Reppert SM, Sassone-Corsi P. 2002 Bimodal regulation of mPeriod promoters by CREB-dependent signaling. J. Theor. Biol. 230, 541 – 562. (doi:10.1016/j.jtbi.2004.04.040)

58. Ohbrient K, Impy S, Smith D, Athos J, Storm DR. 1999 Circadian regulation of αMmp response element-mediated gene expression in the suprachiasmatic nuclei. J. Biol. Chem. 274, 17748 – 17756. (doi:10.1074/jbc.274.25.17748)

59. Brancaccio M, Maywood ES, Chessam JE, Loudon ASJ, Hastings MH. 2013 A Gq-Ca2+ axis controls circuit-level encoding of circadian time in the suprachiasmatic nucleus. Neuron 78, 714 – 728. (doi:10.1016/j.neuron.2013.03.011)

60. Enoto R, Kuroda S, Ono D, Hasan MT, Ueda T, Honma S, Honma K. 2012 Topological specificity and hierarchical network of the circadian calcium rhythm in the suprachiasmatic nucleus. Proc. Natl Acad. Sci. USA 109, 21 496 – 21 503. (doi:10.1073/pnas.1214415110)

61. Zhang EE et al. 2010 Cryptochrome mediates circadian regulation of cAMP signaling and hepatic gluconeogenesis. Nat. Med. 16, 1152 – 1156. (doi:10.1038/nm.2214)

62. Leloup JC, Goldbeter A. 2004 Modeling the mammalian circadian clock: sensitivity analysis and multiplicity of oscillatory mechanisms. J. Theor. Biol. 230, 274 – 318. (doi:10.1016/S0022-5193(03)00017-6)

63. Decroly O, Goldbeter A. 1982 Birhythmicity, chaos, and other patterns of temporal self-organization in a multiply regulated biochemical system. Proc. Natl Acad. Sci. USA 79, 6917 – 6921. (doi:10.1073/pnas.79.22.6917)

64. Tyson JJ, Chen KC, Novak B. 2003 Sniffers, buzzers, toggles and blinkers: dynamics of regulatory and signaling pathways in the cell. Curr. Opin. Cell Biol. 15, 221 – 231. (doi:10.1016/S0955-0674(03)00017-6)

65. Conrad E, Mayo AE, Ninfa AJ, Forger DB. 2008 Rate constants rather than biochemical mechanism determine behaviour of genetic clocks. J. R. Soc. Interface 5(Suppl. 1), 59 – 515. (doi:10.1098/rsif.2008.0046.focus)

66. Myung J, Hong S, Hatanaka F, Nakajima Y, De Schutter E, Takumi T. 2012 Period coding of BM11 oscillators in the suprachiasmatic nucleus. J. Neurosci. 32, 8900 – 8918. (doi:10.1523/JNEUROSCI.5386-11.2012)

67. Inagaki N, Honma S, Ono D, Tanahashi Y, Honma K. 2007 Separate oscillating cell groups in mouse suprachiasmatic nucleus couple photoperiodically to the onset and end of daily activity. Proc. Natl Acad. Sci. USA 104, 7664 – 7669. (doi:10.1073/pnas.0607713104)

68. Evans JA, Leise TL, Castanon-Cervantes O, Davidson AJ. 2013 Dynamic interactions mediated by nonredundant signaling mechanisms couple circadian clock neurons. Neuron 80, 973 – 983. (doi:10.1016/j.neuron.2013.08.022)

69. Noguchi T, Watanabe K, Ogra A, Yamaska S. 2004 The clock in the dorsal suprachiasmatic nucleus runs faster than that in the ventral. Eur. J. Neurosci. 20, 3199 – 3202. (doi:10.1111/j.1460-9568.2004.03784.x)

70. Noguchi T, Watanabe K. 2008 Regional differences in circadian period within the suprachiasmatic nucleus. Brain Res. 1239, 119 – 126. (doi:10.1016/j.brainres.2008.08.082)

71. Koinuma S et al. 2013 Regional circadian period difference in the suprachiasmatic nucleus of the mammalian circadian center. Eur. J. Neurosci. 38, 2832 – 2841. (doi:10.1111/jen.12308)

72. Belle MDC, Diekman CO, Forger DB, Higgins HD. 2009 Daily electrical silencing in the mammalian circadian clock. Science 326, 281 – 284. (doi:10.1126/science.1169657)

73. Buhr ED, Yoo SH, Takahashi JS. 2010 Temperature as a universal resetting cue for mammalian circadian oscillators. Science 330, 379 – 385. (doi:10.1126/science.1195262)

74. Yamauchi S, Isejima H, Matsuo I, Okura T, Yagita K, Kobayashi M, Okamura H. 2013 Synchronization of cellular clocks in the suprachiasmatic nucleus. Science 340, 1408 – 1412. (doi:10.1126/science.1241338)

75. Forger DB. 2011 Signal processing in cellular clocks. Proc. Natl Acad. Sci. USA 108, 4281 – 4285. (doi:10.1073/pnas.1007420108)