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Constraining the duty cycle of transient low-mass X-ray binaries through simulations

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ABSTRACT

We performed simulations of a large number of so-called very faint X-ray transient sources from surveys obtained using the X-ray telescope aboard the Neil Gehrels Swift Observatory on two Galactic globular clusters, and the Galactic Centre. We calculated the ratio between the duty cycle (DC) we input in our simulations and the one we measure after the simulations. We found that fluctuations in outburst duration and recurrence times affect our estimation of the DC more than non-detected outbursts. This biases our measures to overestimate the simulated DC of sources. Moreover, we determined that compact surveys are necessary to detect outbursts with short duration because they could fall in gaps between observations, if such gaps are longer than their duration. On the other hand, long surveys are necessary to detect sources with low DC because the smallest DC a survey can observe is given by the ratio between the shortest outburst duration and the total length of the survey. If one has a limited amount of observing time, these two effects are competing, and a compromise is required which is set by the goals of the proposed survey. We have also performed simulations with several artificial survey strategies in order to evaluate the optimal observing campaign aimed at detecting transients as well as at having the most accurate estimates of the DC. As expected, the best campaign would be a regular and dense monitoring that extends for a very long period. The closest real example of such a data set is the monitoring of the Galactic Centre.

Key words: methods: analytical – methods: data analysis – methods: numerical – methods: statistical – X-rays: binaries.

1 INTRODUCTION

X-ray binaries are constituted of a compact object (a neutron star or a black hole) accreting mass from a companion. If the companion is a relatively low-mass star (typically of the order \( \lesssim 1 \) M\(_\odot\)) then those systems are called low-mass X-ray binaries (LMXBs). Most LMXBs are transient sources: they are usually in a very faint quiescent state but occasionally they show bright X-ray outbursts (for typical outburst light curves, see Chen, Shrader & Livio 1997; Yan & Yu 2015). Wijnands et al. (2006) classified transient LMXBs according to their peak X-ray luminosity (in the energy range 2–10 keV) during outbursts into multiple classes.1 The bright to very bright transients have peak outburst luminosities of \( 10^{37–39} \) erg s\(^{-1}\). Due to their brightness those systems are readily discovered and have been intensively studied over the last four decades. Therefore, we have a good understanding of their behaviour.

Faint and very faint X-ray transients (VFXTs) have peak X-ray luminosities of \( 10^{30–37} \) and \( 10^{34–36} \) erg s\(^{-1}\), respectively. Their faintness makes outbursts of those systems significantly more difficult to discover compared to those of the brighter transients because the resulting fluxes are typically low to very low and often below the sensitivity of X-ray all-sky monitors (ASMs) orbiting the Earth. This problem is of course most severe for the VFXTs and such systems are typically discovered serendipitously when sensitive X-ray satellites (e.g. Swift, Chandra, and XMM–Newton) are pointed at certain sky positions in the Galaxy (for early examples of the discovery of VFXTs, see e.g. Hands et al. 2004; Mun\o et al. 2005; Porquet et al. 2005) or at Galactic globular clusters (e.g. Heinke et al. 2009b; Heinke 2010). To increase the probability of finding new VFXTs and detecting more outbursts of the known systems, several optimized observing campaigns have been performed both for the Galactic Centre region (Wijnands et al. 2006; Degenaar...
and references therein). The current leading model to explain the mechanism behind the outbursts of transient LMXBs is the disc instability model (DIM; for an extensive review on the DIM, see Lasota 2001). Between the outbursts, the material supplied by the companion star is stored in the relatively cool disc surrounding the compact object. This eventually leads to a thermal instability which results in the increase of the viscosity and therefore the accretion rate onto the compact object resulting in a X-ray outburst. Currently, it is not yet clear if the DIM can also explain the outburst of the VFXTs, but Hameury & Lasota (2016) argued that indeed the DIM could explain those systems if they are so-called ultracompact X-ray binaries which are systems with a very small orbital period of \(\lesssim 90\) min and have hydrogen poor accretion discs.

The duty cycle (DC) of a transient source is expressed as the ratio between the time spent in outburst and the time interval between the start of two consecutive outbursts (thus the recurrence time of the outbursts). Both the outburst and the recurrence times are very important ingredients in the DIM (see details in Lasota 2001), so determining accurate DCs is crucial to constrain and test the DIM. Determining accurate DCs is important for several other reasons as well. Using the DC and the averaged mass accretion rate during outbursts (which can be obtained from the averaged source luminosity in outburst in combination with the source distance), we can obtain the averaged (over the outburst and quiescent period; assuming no accretion at all takes place in quiescence) mass accretion rate \(\langle \dot{M}_A \rangle\). Since the historical outburst behaviour of X-ray transients is only known for years to at most several decades, this average can only be calculated from the observational data for a similar time span. Therefore, we have to assume that this estimate is representative for the mass accretion rate over time-scales as long as \(\sim 10^{4-5}\) yr. For such long periods, \(\langle \dot{M}_A \rangle\) can be assumed to be equal to the mass transfer rate \(\langle \dot{M}_{\text{TF}} \rangle\) from the companion star (assuming conservative mass transfer; thus any mass loss due to outflows, like jets or winds, is assumed to be negligible). This \(\langle \dot{M}_{\text{TF}} \rangle\) is an important parameter in X-ray binary evolution models (see e.g. the review by Tauris & van den Heuvel 2006) as well as population synthesis models of LMXBs (e.g. van Haften et al. 2013, 2015, and references therein).

In addition, determining an accurate \(\langle M_A \rangle\) (and thus obtaining accurate DCs) is also important in several studies involving neutron star physics. For example knowing \(\langle M_A \rangle\) is crucial in understanding how neutron stars are heated due to accretion of matter and cool when the accretion has halted (e.g. Brown, Bildsten & Rutledge 1998; Colpi et al. 2001; Yakovlev & Pethick 2004; Wijnands et al. 2008; Heinke et al. 2009a; Wijnands, Degenaar & Page 2013, 2017; Ootes, Wijnands & Page 2019). Determining an accurate \(\langle M_A \rangle\) is also very important in understanding the magnetic field evolution in accreting neutron stars, both for the long-term evolution (Taam & van den Heuvel 1986; Romani 1990; Geppert & Urpin 1994) as well as for possible short-term screening of the magnetic field by the accreted matter, and why some neutron-star LMXBs exhibit millisecond pulsations and others do not (e.g. Cumming, Zweibel & Bildsten 2001; Galloway 2006; Wijnands et al. 2008; Patruno 2012; Patruno & Watts 2012). Finally, knowing \(\langle M_A \rangle\) accurately is important to determine the physical reason why the spin distribution of neutron stars appears to have a cut-off at about \(\sim 730\) Hz (e.g. Chakrabarty et al. 2003; Patruno, Haskell & D’Angelo 2012; Papitto et al. 2014).

We have relatively good constraints on the DC of the bright and very bright transients because their outbursts are detectable with ASMs, and many of them have exhibited multiple outbursts. Typically, the DC of those transients is in the range 0.01–0.1, with an average value of \(\sim 0.03\) (see e.g. fig. 10 in Yan & Yu 2015). We note that those DCs are determined over a time span of about 15 yr, and it is not necessarily true that they are representative for the long term (i.e. evolutionary time scales) DCs of those systems. This short time span introduces a detection bias for systems that have large DCs because those systems are more likely to have multiple detected outbursts, and therefore that their DCs can be constrained.

Due to the difficulties in detecting outbursts of faint X-ray transients and VFXTs, many of those outbursts are missed, significantly hampering the determination of the DCs for those systems (again this is most severe for the VFXTs). Based on 4 yr of Swift/X-ray telescope (XRT; Gehrels et al. 2004) monitoring of the Galactic Centre, Degenaar & Wijnands (2010) found a large range of DCs for the detected VFXTs in their survey, ranging from DCs of only a few per cent (see also Degenaar et al. 2015) to DCs above 50 per cent.

For this reason, the DCs of VFXTs appear very similar to that of the brighter transients (see Yan & Yu 2015). Constraining accurate DCs for the VFXTs might also help to differentiate the different potential sub-types of VFXTs (see Wijnands et al. 2006) from each other, although investigating this is beyond the scope of our current paper.

The observing campaigns in which outbursts of VFXTs are typically detected are very infrequent, often not regularly spaced in time, and often with very large time span between observations. It is thus likely that the calculated DCs (or the upper limits on the DCs) for many VFXTs have large uncertainties. The aim of this paper is to investigate how the accuracy of the DCs of VFXTs is affected by the properties of the observing campaigns.

Several existing observing campaigns can be used for our study. For example, the Galactic Centre has been very frequently monitored (nearly once every day for \(\geq 10\) yr now; Degenaar & Wijnands 2010; Degenaar et al. 2013b, 2015) using the XRT aboard Swift. Several VFXTs have indeed been detected, in some case even with multiple outbursts (see e.g. the summary given in Degenaar et al. 2015). In addition, several observing campaign (e.g. using RXTE or Swift/XRT; Altamirano et al. 2011; Wijnands et al. 2012; Linares & Chenevez 2016) on Galactic Globular cluster systems have been preformed to find X-ray transients, since a sizable number of those clusters are expected to host multiple transient LMXBs (e.g. Heinke et al. 2003; see table 5 of Bahramian et al. 2014 for a list of active, both persistent as well as transient, LMXBs in globular clusters). Therefore, pointed observations using sensitive X-ray instrumentation of those clusters will allow to monitor several systems at once increasing the likelihood that outbursts are discovered. Because of the sensitive of the XRT in combination with the flexibility of Swift, this satellite is currently most often used to obtain such pointings (as well as pointings at the Galactic Centre). For this reason, in our simulations we focus only on observing campaigns performed with Swift/XRT.

\[2\]Several VFXTs with such high DCs are known (Del Santo et al. 2007; Degenaar & Wijnands 2010; Arnason et al. 2015) and are commonly referred to as quasi-persistent transients (see e.g. Remillard 1999, who was the first, to our knowledge, who called these transients this way) which are transient LMXB that have very long, up to decades, outbursts. Examples of quasi-persistent transients can be found in all luminosity classes defined in this paper.
Beside using the sampling of existing campaigns we will also investigate if we can determine what kind of observing strategy would constrain the DCs best, while maximizing the detection of outbursts (thus allowing us to determine the optimal observing strategy to discover more VFXTs). We will discuss the Swift/XRT observing campaign we use in Section 2; in Section 3, we present the methods used to perform our simulations. We will then present the results of our investigation in Section 4 and discuss their implications and conclude in Section 5.

2 OBSERVING STRATEGIES

Using Swift/XRT,3 a number of Globular clusters have been monitored frequently, either to find more transients (Wijnands et al. 2012; Linares & Chenevez 2016) or to monitor detected transients during their outbursts (e.g. Del Santo et al. 2014; Bahramian et al. 2014; Linares et al. 2014; Tetarenko et al. 2016). Those campaigns are excellent input for our simulations because they demonstrate directly what is possible using Swift/XRT, and are therefore representative of the accuracy one can obtain on the DCs. From the clusters monitored with Swift/XRT, we decided to use the observations from NGC 6388 (discussed in Section 4.1), and Terzan 5 (discussed in Section 4.2).

NGC 6388 was chosen because it only had a three month period during which it was monitored about once a week. The separation between consecutive observations is smaller than the minimum outbursts duration we have assumed in our simulations (see Section 3), implying that it is very unlikely that a simulated outburst occurring during the input observing campaign would not be detected. On the other hand, the time span of this survey is very limited, making it very difficult to recover transients with a low DC. Terzan 5 was chosen because the observations cover a relatively long time span of 4.5 yr, with episodes of dense sampling, but also with large gaps between observations. These gaps range between a few days, and almost 2 yr. The presence of long gaps will likely cause many outbursts to be non-detected, allowing us to determine the effect of this on the accuracy of the observed DCs.

The observing campaign on these clusters are quite different, allowing us to investigate the effects of those different strategies on the obtained DCs. We note that we use those campaigns only as sampling strategy; whether or not a source was detected (or even monitored) during those observations is irrelevant for the purpose of our paper. Table A1 summarizes the observing dates that were used in the simulations for the surveys of NGC 6388 and Terzan 5, highlighting the difference between the two.

The observing campaign of the Galactic Centre includes a total of 1682 observations (due to the very large number of observations we do not include them in Table A1), covering a period between 2005 October and 2017 November with gaps of about three months between November and February due to Solar constraints. This is the best Swift/XRT data set for a single position in the sky because it has a long baseline and a very dense coverage.

3http://www.swift.ac.uk/swift_portal/index.php

3This is true because the quantity that affects the DC the most is the amount of matter that is accreted during an outburst. In fact, this would affect the duration of the following quiescence period, because it would take the source a different amount of time to replenish its accretion disc. The amount of matter that is accreted is mostly determined by the peak luminosity and the duration of an outburst, rather than by the exact light-curve shape (as far as it is not radically different).
the start time the next outburst of the same source, and if this time is lower than the end of the survey, the following outburst will be simulated in the same manner. This way we produced a catalogue with simulated sources, each of which is constituted by multiple outbursts, and has a certain value of the DC.

We also have to input a survey strategy for which we used the previously mentioned observing campaigns (see Section 2). The most important information needed from those campaigns is the start time of the observations. Our code also requires to input the integration time and the sensitivity of each observation (see Carbone et al. 2017). The sensitivity of our observations is determined by our instrument, in this case Swift/XRT. For sources at the distance of the targets we chose to simulate (NGC 6388, Terzan 5, and the Galactic Centre), Swift/XRT is sensitive enough to detect sources until they enter the quiescence period, i.e. when their luminosity drops below $10^{34}$ erg s$^{-1}$ (Plotkin, Gallo & Jonker 2013; Wijnands et al. 2015). We therefore define the limit for when a source is in outburst as to when its luminosity is above $10^{34}$ erg s$^{-1}$.

The integration time is less important because most of the outbursts have peak luminosity much larger than the sensitivity limit, but it is still relevant because some of them might be detectable only during the decay phase, and their signal might be smeared out in the background noise in long observations.

This list of simulated sources is then checked against the survey strategy to test if each of the outburst we simulated is detected or not. This is done by checking if the outburst was active during each observation (i.e. if it was bright enough to be detected). This way we produced a catalogue of the simulated sources that were detected at least once; for each source a different number of outbursts have been detected. After this, we calculated the DC for each of the sources that were detected at least twice, so we can compare it to the input DC. This calculation is performed as explained in Section 4. We calculated a value of the DC for each pair of consecutive detected outbursts. The DC of a source for which many outbursts are detected is calculated both as the maximum and as the average of the calculated DCs. We chose to calculate both because if an outburst from one such source has not been detected, the average DC would be strongly biased towards lower values, whereas the maximum would still be as close as possible to the real one. On the other hand, the maximum would be systematically biased towards larger values, not representing the real value as well as the average, if the latter is not dramatically affected by missing outbursts. Our simulations only consider sources that exhibit at least one outburst during the considered observing campaign because we are interested in testing how obtained DCs compare to the input DCs, i.e. we want to test how accurate the measurements of DCs from real data are and in what way they could be biased.

4 RESULTS

We define the value of DC that was inputted in our simulations as $\text{DC}_{\text{sim}}$ (the simulated DC) and the value of DC that is calculated from the catalogue of the detected sources as $\text{DC}_{\text{obs}}$ (observed DC, although observed in this context means determined from our simulated data sets and not obtained from actual observations). $\text{DC}_{\text{obs}}$ is calculated using equation (1), where the numerator, indicating the duration of outburst $i$ ($T_{\text{outburst},i}$), is derived from the observations, i.e. it is the time difference between the first and last detections of such outburst. This value is different from the simulated duration of that event because an outburst might not be detected as soon as it starts, and might not be observed as it fades away completely. The denominator, indicating the interval between the first detections of two consecutive detected outbursts $i$ and $i + 1$, is also derived from the observations (i.e. from our simulated datasets). This value can be different from the simulated one both because an outburst might not be detected as soon as it starts, and because outbursts might end up being non-detected at all, strongly affecting this calculation (i.e. two consecutive detected outbursts might not be two consecutive simulated outbursts). A consequence of how we modelled the DC and the duration of the outbursts, $\text{DC}_{\text{obs}}$ can be as high as four times $\text{DC}_{\text{sim}}$ because both the numerator and the denominator of equation (1) can vary by up to a factor of 2. We repeated our simulations allowing the duration of the outbursts to vary by a factor of 3 instead of 2, and then the maximum $\text{DC}_{\text{obs}}$ was indeed six times $\text{DC}_{\text{sim}}$ as expected. In future work, we will include a probability distribution on those quantities in our code and this could change the maximum ratio between $\text{DC}_{\text{obs}}$ and $\text{DC}_{\text{sim}}$, however, we expect this will not change the main conclusions of our paper.

As previously mentioned, due to our simulation setup there are sources that are in outburst before the campaign started and do not repeat while it is ongoing; those sources are excluded when calculating the probabilities discussed below.

4.1 NGC 6388

For our first simulations, we used the Swift/XRT observing campaign of NGC 6388 as our survey strategy. The results of those simulations are shown in Fig. 1. The detection probability discussed here and for the rest of the manuscript is defined as the ratio between the number of detected sources with a certain value of $\text{DC}_{\text{sim}}$ (or other variables) and the total number of simulated sources with the same $\text{DC}_{\text{sim}}$ (or other variables). As mentioned earlier, only sources that exhibit at least one outburst during the observing campaign are taken into account in this calculation. A source is detected if at least one outburst is detected. We calculated the probability of detecting transient sources as a function of their $\text{DC}_{\text{sim}}$ (see top left panel of Fig. 1) and found that it is very high ($\sim 1$) for all the values of DC. This is due to the fact that every outburst that occurs during the campaign is detected thanks to the compactness of the campaign. Only very few outbursts are missed, those that have only a small portion happening during an observation. We also observe that there is a scatter especially at low values of DC. This is due to the fact that for such low values, only one outburst occurred during the observing campaign. If this outburst was not detected, then the whole source was not, and therefore it does not show up in the plot, whereas for higher values of DC, if one outburst was missed, another one from the same source could still have been detected, increasing the probability that the source is detected.

We also calculated the probability of detecting sources as a function of the average duration of their outbursts. We note that almost all sources were detected, with a probability of detection of 1 for almost all durations. Only very short outbursts are sometimes non-detected. This is due to the fact that outbursts shorter than 14 d may appear in only one observation and, for the shortest, their luminosity might have dropped below $10^{34}$ erg s$^{-1}$ at the time of the observation. This is shown in the top right panel of Fig. 1.

We then identified and selected sources that have multiple detected outbursts. From the middle left panel of Fig. 1, we can see that almost all sources exhibiting an outburst during the observing campaign have been detected at least one, but also that only a minority of sources have been detected multiple times. All the multiple detections belong to sources with $\text{DC}_{\text{sim}} \geq 0.04$. These effects (all sources are detected, but only a minority multiple times)
Figure 1. Results of our simulations using the observing campaign of NGC 6388 as input survey strategy. Only sources exhibiting at least one outburst during the observing campaign are presented in this analysis. The top left panel shows the probability of detecting a source as a function of its DC$_{\text{sim}}$; and the top right panel shows the probability of detecting an outburst as a function of its duration. The middle left panel represents a cumulative histogram of all simulated sources colour coded based on the number of outbursts that were detected. The green line in that plot (visible at the very bottom in this case), represents the probability that a source would never be detected (i.e. all outbursts from that source would not be detected) as a function of its DC$_{\text{sim}}$. The middle right panel represents a cross-cut at DC$_{\text{obs}}$ = 0.10 in the bottom right panel. It shows how accurate our estimation is. The bottom panels show, colour coded, the probability that a source has a certain simulated DC (DC$_{\text{sim}}$) provided that the observed value (DC$_{\text{obs}}$) is another. The sum of the probability is one in each vertical bin. The black dots in the bottom panels represent the average value of the simulated DC for different observed ones. In the bottom left panel, DC$_{\text{obs}}$ is calculated as the maximum from different outburst pairs, while in the bottom right panel, it is calculated as the average. The black line in both bottom panels represents the ideal one-to-one relation.
are due to the very dense coverage of the observations, and to the very short duration of the campaign, respectively. We have simulated an even number of sources per DC bin. The sources missing from the bins with low DC in this panel are the ones that do not exhibit any outburst during the observing campaign and are therefore excluded from this analysis. This effect is not a surprise as sources with low DC are rarer, and therefore if the first outburst we simulated happened before the campaign started, then the following one would happen only after the same campaign was over, and as the observations of NGC 6388 lasted only for a few months, several sources suffered this effect. This will be very different for different strategies as highlighted in the remainder of the manuscript. The green line in the same plot represents the probability that a source would not be detected with this observing campaign, i.e. all of the outbursts from this source would not be detected. In the case of NGC 6388 this probability is very small, lower than 2 per cent for all values of the DC. This quantity depends a lot on the observing strategy, and will be very different for different campaigns.

Finally, we compared DC_{obs} with DC_{sim}, both when DC_{obs} is calculated as the maximum and when it is calculated as the average of the observed DC for each source. The two cases are represented in the bottom left and bottom right panels of Fig. 1, respectively. For different values of DC_{obs} we calculated the probability that such value corresponds to specific DC_{sim}, i.e. we considered all sources having a certain value of DC_{obs} and compared it to their DC_{sim}. The black line represents the ideal one-to-one relation. We note that the two plots look similar because almost all sources have at most two detected outbursts, meaning that the maximum and the average DC_{obs} are the same. For almost all values of DC_{obs} it is possible to both overestimate and underestimate DC_{sim}. In order to quantify this discrepancy, we show in black dots the average value of DC_{obs} for each bin of DC_{sim}, and we note that the average DC_{obs} is systematically larger than DC_{sim}, despite having a large scatter. This is more clearly visible in the middle right panel of Fig. 1, where we performed a cross-cut at DC_{obs} = 0.10 in the bottom right panel (the one using the average DC_{obs}). From this plot we see that there are more sources for which we overestimated their DC, rather underestimating it. This is expected, as we can more easily detect outbursts from sources which have more frequent outbursts than the average. We remind that we introduced a factor of 2 scatter in the DC.

4.2 Terzan 5

We have performed the same analysis for the globular cluster Terzan 5, which has a rather different observing campaign than NGC 6388 (see Section 2). The outcome of our simulations is presented in Fig. 2. In the top left panel, we can see that in this case the probability of detecting sources as a function of their DC_{sim} goes from about 0.4 for very low values of DC_{sim}, reaching 1 for the highest values of DC_{sim}. Similar to our simulations of NGC 6388, this is due to the fact that more frequently recurring sources (i.e. high DC) exhibit more outbursts during the observing campaign, increasing the probability of detecting at least one. The probability to detect simulated outbursts as a function of their duration is plotted in the top right panel of Fig. 2. Here, the probability of detection remains above 0.8 for all values of the duration, but does not stay constant at 1 for long outbursts. This plot is very different than the one observed for NGC 6388 and is due to the presence of long gaps (> 200 d) between consecutive observations. Sources of all durations might go into outburst during a gap and such outburst, if too short, might not be detected. If such outburst is the only one happening during the campaign the whole source will never be detected, whereas if the recurrence time is shorter, other outbursts could compensate for such eventuality. This implies that most of the sources that are not detected have low DC_{sim}, as visible in the middle left panel.

On one hand, the presence of long gaps cause some sources to end up non-detected, most of which have small DC_{sim}. On the other hand, the long duration of the observing campaign allows for a large number of sources to have multiple detected outbursts. In the case of Terzan 5, the probability that a source would not be detected reaches values above 50 per cent for sources with very small DCs, and decreases monotonically, as already mentioned.

In the case of the observing campaign of Terzan 5, the two bottom panels are more diverse compared to the campaign of NGC 6388. The spread of the colour area, as well as the error bars on the black dot are larger in the bottom left panel, where DC_{obs} is calculated as the maximum, compared to the bottom right panel (where DC_{obs} is calculated as the average). Also for Terzan 5, DC_{obs} can both be an overestimation or an underestimation of DC_{sim}, but the overestimations are more common, as highlighted by the positions of the black dots, and by the middle right panel in Fig. 2.

4.3 The Galactic Centre

In Fig. 3, we show the results of our simulations using the Swift/XRT observing campaign of the Galactic Centre. This survey combines the positive things of the previous two: it lasted for more than a decade, enabling many sources to have multiple detected outbursts, and had very frequent observations, without long gaps (apart from the Solar impediments), avoiding most outbursts to fall in these periods.

As can be seen from the top left panel of this figure, most sources are detected. Only sources with simulated DC smaller than ~ 0.02 have about 10–20 per cent probability of not being detected. This implies that all the transients near the Galactic Centre with DC higher than 0.02, which underwent an outburst during the observing campaign, must have been detected (within our assumptions on the sources properties such as outburst duration). Moreover, if a new source exhibits its first outburst after the current observing campaign, it can have a maximum DC of \( D_{\text{max}} = \max(T_{\text{outburst}}/T_{\text{survey}}) \leq 0.05 \), where \( T_{\text{survey}} \) is the duration of the survey (~10 yr). This implies that all the transient sources which exhibit outbursts with durations between 7 and 200 d and have a DC larger than 0.05 have been detected already.

We note that sources that exhibit very long outbursts (e.g. > 1 yr; the so-called quasi-persistent sources; see footnote 2) and have DC < 0.1 would have quiescent periods > 10 yr and therefore they could have still remained undetected by this survey. Another type of transient that might be missed with this survey campaign would be the one having periodic outbursts with recurrence time almost exactly multiple of a year, with outbursts all coinciding with the gap in the observations due to Solar constraints, and duration shorter than that gap.

In the top right panel of Fig. 3, we can see that all outbursts have close to 100 per cent probability of being detected regardless of their duration. This means that DC is the only variable playing a role in the detectability.

As mentioned, most sources are detected multiple times with this strategy, and very few outbursts are actually missed. This reflects in the middle left and the two bottom panels of Fig. 3. In the middle left panel, we can also see that the probability of a source not
being detected at all is never higher than 10 per cent. In the two bottom panels, if we estimate $D_{\text{C,obs}}$ as the maximum, on the left, we largely overestimate $D_{\text{C,obs}}$ as our measurements are biased by the fluctuations in DC that we simulates (as described in Section 3). On the other hand, if we use the average value, we only slightly overestimate $D_{\text{C,obs}}$, with quite narrow error bars. This is confirmed also looking at the middle right panel, where we clearly see that for most sources with $D_{\text{C,obs}} = 0.10$ we are overestimating their DC by about 10 per cent.

4.4 Different survey strategies

We have performed simulations for several artificial observing campaigns to determine what kind of strategies would optimize
the detection of transients, and would result in the most accurate estimation of their DCs. For the total observing time of those artificial strategies, we have chosen the one of the Terzan 5 campaign (total observing time of $\sim 58$ ks) as a representative sample for what can be obtained with Swift/XRT. We divided this in 58 observations of equal duration of 1 ks.

We then spaced these observations in different ways: one week apart (similar to the strategy used for NGC 6388), one month apart, three months apart and, logarithmically spaced. For the last strategy, we divided the observations in blocks of seven observations. The observations within the same block are uniformly spaced, but separated by different amounts in different blocks. The separations of the date.

**Figure 3.** Results of our simulations using the observing campaign of the Galactic Centre as input observing campaign. The six panels are the same as in Fig. 1.
we used are 1 d, 4 d, 7 d, 14 d, 1 month, 3 months, 6 months, and 1 yr. The separation between the last observation of a block and the first of the following is set equal to the separation between observations of the latter. While the total exposure time is constant, the length of the observing campaign is different for each of the strategies, ranging between 398 d (∼1 yr) for the most compact one and 5292 d (∼14.5 yr) for the logarithmically spaced strategy. The results of our simulations are shown in Figs 4 and 5.

In the left-hand panels of Fig. 4, we show the same plot as in the bottom right panel of Fig. 1, while in the right ones we show the same plot as in the middle left panel of Fig. 1. Observing the left-hand panels in Fig. 4, we note that in all cases DCsim is slightly overestimated and that the error bar we find shrink for longer and longer campaigns. In the right-hand panels of Fig. 4 we can instead observe that going from spacing of 1 week to 1 month, and then to 3 months we are able to detect more and more sources and more and more sources are detected multiple times (i.e. we were able to measure their DCobs). The logarithmically spaced strategy is constituted by an initial cluster of very close spaced (in time) observations that become less and less frequent, and in the second half of the survey observations are a year apart. This causes many outbursts to be undetected and therefore many sources with a small DCsim are not detected because their few (or only) outbursts end up during the very long gaps in this campaign. These effects are clear in the bottom right panel of Fig. 4. We also note a dramatic change in the probability of completely missing a source as a function of its DC. This probability is extremely small with observations spaced 1 week from one another (<1 per cent), it reaches about 30 per cent when they are 1 month apart, 50 per cent if they are 3 months apart, and 75 per cent in case they are logarithmically spaced.

We compared the results of these surveys in Fig. 5. In the left-hand panel, we show the probability of detecting a source as a function of its DCsim for different artificial strategies. We note that the most compact strategy (marked with black stars) can detect basically all sources undergoing an outburst during the observing campaign. The probability of detecting sources decreases steadily as the gap between consecutive observations increases from 1 week, to 1 month, to 3 months. The survey strategy with observations logarithmically spaced is the one that has the lowest probability of detecting sources. This is due to the fact that it has very large gaps between consecutive observations in the latter part of the campaign. This is the reason why dense campaigns are at an advantage.

In the right-hand panel of Fig. 5, we show the same as on the left-hand panel, but restricting the sample to only those that had two or more detected outbursts during the observing campaign. Here, it is clear that each survey can observe multiple outbursts from sources only down to a limit DC that is related to the total length of such survey. The smallest DC a survey can observe is given by the ratio between the shortest outburst duration and the total length of the survey. This is the reason why long campaigns are at an advantage.

In the bottom panel of Fig. 5, we show the probability of detecting outbursts as a function of their duration. We can see that each survey has a probability of 1 of detecting outbursts longer than the longest gap in them. Outbursts shorter than that are only occasionally detected, and the probability of detecting such outbursts is directly proportional to their duration, as shown in Carbone et al. (2017).

4.5 Single outbursts detections

Finally, we have tested whether we could constrain in any way the DC of sources for which only one outburst was detected in our simulations using the artificial survey strategies as discussed in Section 4.4. Our approach to this problem is the following: for all sources with a single detected outburst, we have calculated the time at which an outburst with the same duration could have started and not have been detected. This could be either before our campaign started, after the campaign ended, or in a gap long enough during the campaign itself. In all three cases we calculated what the corresponding DC would have been, and we selected the largest obtained value. We have estimated the duration of a source as the time difference between the first and last detections. An example of the results from this analysis is shown in Fig. 6 for the strategy in which the observations are spaced by one week. It is clear that provided we estimate a certain value for DCobs in case of a single detection, this does not allow us to reconstruct the simulated value of the DC.

5 DISCUSSION AND CONCLUSIONS

Using an expanded version of the transient simulation code of Carbone et al. (2017), we have simulated the X-ray light curves of outburst from transient LMXBs to investigate the bias that an observing campaign can introduce in the calculation of DC of these sources, and in particular we focused on the VFXTs.

In our simulations we used as input survey strategy, the Swift/XRT observing campaigns of the globular clusters NGC 6388 and Terzan 5, and the very extensive campaign on the Galactic Centre. Those campaigns were chosen because they give us a good variety in density of the observation sampling, and the total duration of the campaigns. Therefore, our results should be directly applicable to those, and to similar observational strategies. From our simulations of the survey of the Galactic Centre, we determined that all the transient LMXBs in that region, with DC larger than 0.02, undergoing at least an outburst during the observing campaign have been detected. Moreover, if a new source will exhibit its first outburst since the beginning of the monitoring campaign, it will have a DC smaller than 0.05, if the duration of the previous outburst was smaller than 200 d. This implies that all the transient sources with outbursts shorter than 200 d, and DC higher than 0.05 have been already detected. However, quasi-persistent sources, which have very long outbursts (> 1 yr), could still have remained undetected despite they might have higher DCs, because of their very long quiescence period that could extend longer than the campaign has been active. Another type of transient that might be missed with this campaign would be the one having periodic outbursts with recurrence time almost exactly multiple of a year, with outbursts all coinciding with the gap in the observations due to Solar constraints, and duration shorter than that gap.

From our simulations, it is clear that fluctuations in outburst duration and recurrence times affect our estimation of the DC more than non-detected outbursts. This biases our measures to overestimate the simulated DC of sources. The next step in such simulations is to model fluctuations in both the outburst duration and the recurrence time with Gaussian distributions. Since real transients have also a variation in their outburst duration and the duration of their quiescence period (e.g. see Yan & Yu 2015), determining the DC of those transients (see Degenaar & Wijnands 2010, for the DC of VFXTs and Yan & Yu 2015 for the DC of the brighter transients) will very likely also suffer this bias. We note that despite we performed our simulations with a focus on VFXTs, very likely this conclusion (i.e. DC calculations being affected more by fluctuations in outburst duration and recurrence times rather than undetected outbursts) applies for brighter transients as well.
Figure 4. Plot of the bottom right and middle left panels as in Fig. 1 for the four artificial survey strategies described in Section 4.4. All of the strategies are composed of 58 observations of 1 ks. From top to bottom, the observations are one week, one month, three months apart, and logarithmically spaced.
Figure 5. Plot of the probability of detecting simulated sources as a function of their simulated DC, for all sources in the top left panel, and only for sources exhibiting multiple outbursts during the observing campaign in the top right panel. The vertical lines in the right-hand panel represent the minimum DC different artificial surveys can measure. The bottom panel shows the probability of detecting outbursts as a function of their duration. The vertical lines in the bottom panel represent the longest gap between two consecutive observations in different artificial surveys.

Figure 6. Same plot as in the left-hand panels in Fig. 4 for the artificial strategy with observations one week apart, but plotting only sources with only one detected outburst. It is clear that in this case we cannot gather any information on DC_{sim} given we estimated DC_{obs} from a single outburst detection.

From our analysis of the probability of detecting individual sources, we have determined that compact surveys are necessary to detect outbursts with short durations because we showed that a survey is detecting all sources with duration longer than the maximum separation between consecutive observations, while the detection probability decreases for shorter and shorter outbursts. On the other hand, long surveys are necessary to detect sources with low DC because the smallest DC a survey can observe is given by the ratio between the shortest outburst duration and the total length of the survey. If one has a limited amount of observing time these two effects are competing, and a compromise is required which is set by the goals of the proposed survey.

In order to investigate what the best observing campaign would be to maximize the probability to detect transients as well as to have the most accurate estimates of the observed DC, we have also performed simulations with several different artificial survey strategies (see Section 4.4 for details). As expected, the best campaign would be a regular monitoring that extends for a very long period, without any long gap between observations. The closest real example of such a data set is the monitoring of the Galactic Centre.

We have simulated artificial surveys with regular separations between consecutive observations of 1 week, 1 month, and 3
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Astrophysics Data System Bibliographic Service.

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months. We have also simulated a survey composed of blocks with observations logarithmically spaced. As expected, we found that the survey with observations 1 week apart is the one that give the highest probability of detecting individual sources (i.e. detecting at least one outburst from a source if it was active during the observing campaign, see Fig. 5). We determined that the survey with logarithmically spaced observations is the one that has the lowest probability of detecting transients, despite it can probe lower values of the simulated DC. Such survey resembles strategies in which a target field was observed with a dense sampling for a certain period and then it gets a few sparse observations later on. We have shown how such approach might not lead to any further constraints on the DCS, nor increase significantly the likelihood of detecting new transients. A better strategy would be to initiate a new dense monitoring of the same region rather than have few individual points per year.

We have shown that the minimum DC that can be determined using a specific survey is a function of its total duration, as longer surveys can probe lower DCS, and as most of the DCS for real transients are below 0.1, a survey of duration of at least months is required to probe that regime. We have also proved that very dense surveys, with observations every a few days, will not miss (almost) any outburst and will therefore not be affected by the issue of underestimating the DC, assuming that the observing campaign lasts at least one full cycle (outburst plus quiescence).

An expansion to our simulation code would be to also include the calculation of $\langle M_A \rangle$. As explained in the Introduction, $\langle M_A \rangle$ is very important for binary evolution and population models, as well as to study certain types of neutron star physics. Finally, another possible development of our simulations would be the inclusion of different distributions of the variations in DC and outburst duration.

APPENDIX A: LIST OF THE OBSERVATIONS

In Table A1, we report the dates of all the observations we used in our simulations regarding the campaigns on Terzan 5 and NGC 6388.

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Table A1. Summary of the dates of the existing Swift/XRT observations of the globular clusters Terzan 5 and NGC 6388 that were used as input observing campaign in our simulations.

|        | Terzan 5 |                | NGC 6388 |                |
|--------|----------|----------------|----------|----------------|
| 2010-10-28 | 2015-03-21 | 2016-04-21 | 2012-06-02 |                |
| 2010-10-31 | 2015-03-23 | 2016-04-23 | 2012-06-09 |                |
| 2011-10-26 | 2015-03-25 | 2016-04-29 | 2012-06-16 |                |
| 2012-02-09 | 2015-03-26 | 2016-04-30 | 2012-06-23 |                |
| 2012-06-11 | 2015-03-27 | 2016-05-01 | 2012-06-30 |                |
| 2012-06-16 | 2015-04-02 | 2016-05-15 | 2012-07-08 |                |
| 2012-06-21 | 2015-04-06 | 2016-05-29 | 2012-07-14 |                |
| 2012-06-26 | 2015-04-12 | 2016-05-30 | 2012-07-18 |                |
| 2012-06-30 | 2015-04-13 | 2016-06-12 | 2012-07-21 |                |
| 2012-07-06 | 2015-04-14 | 2016-06-26 | 2012-07-28 |                |
| 2012-07-07 | 2015-04-20 | 2016-06-29 | 2012-08-08 |                |
| 2012-07-08 | 2015-04-22 | 2016-07-10 | 2012-08-11 |                |
| 2012-07-10 | 2015-04-24 | 2016-07-13 | 2012-08-18 |                |
| 2012-07-12 | 2015-04-26 | 2016-07-24 | 2012-08-25 |                |
| 2012-07-13 | 2015-04-28 | 2016-08-07 | 2012-09-01 |                |
| 2012-07-16 | 2015-05-02 | 2016-08-21 | 2012-09-08 |                |
| 2012-07-16 | 2015-05-04 | 2016-09-28 |            |                |
| 2012-07-17 | 2015-05-10 | 2016-10-02 |            |                |
| 2012-07-21 | 2015-05-18 | 2016-10-10 |            |                |
| 2012-07-26 | 2015-05-23 | 2016-10-14 |            |                |
| 2012-08-01 | 2015-05-26 | 2016-10-18 |            |                |
| 2012-08-05 | 2015-06-05 | 2016-10-22 |            |                |
| 2012-08-10 | 2015-06-09 | 2016-10-26 |            |                |
| 2012-08-11 | 2015-06-12 | 2016-10-30 |            |                |
| 2012-08-13 | 2015-06-15 | 2017-04-19 |            |                |
| 2012-08-13 | 2015-06-18 | 2017-05-03 |            |                |
| 2012-08-14 | 2015-06-21 | 2017-05-17 |            |                |
| 2012-08-15 | 2015-06-24 | 2017-05-31 |            |                |
| 2012-08-19 | 2015-06-27 | 2017-06-14 |            |                |
| 2012-08-20 | 2015-06-29 | 2017-06-28 |            |                |
| 2012-08-24 | 2015-07-02 | 2017-07-12 |            |                |
| 2012-08-30 | 2015-07-06 | 2017-07-26 |            |                |
| 2012-09-07 | 2015-07-09 | 2017-08-08 |            |                |
| 2012-09-14 | 2015-07-12 | 2017-08-23 |            |                |
| 2013-05-14 | 2015-08-10 |            |            |                |
| 2015-03-17 | 2016-04-17 |            |            |                |

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