The Effect of Disc Surface Topography on the Dry Gross Fretting Wear of an Equal-Hardness Steel Pair

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Abstract: Experimental investigations were carried out with an Optimol SRV5 tribological tester in a flat-on-sphere scheme. The balls co-acted with the discs in a gross sliding fretting regime. The balls and discs were made from the same steel with a very similar hardness. Tests were conducted at 25–35% relative humidity, 30 °C, and a constant normal load and number of cycles (18,000). The discs had different textures after various machining treatments. It was found that the total wear level of the tribological assembly was proportional to the disc surface amplitude. The influence of the disc roughness on the coefficient of friction was evident only for the smallest stroke of 0.1 mm, and the frequency of oscillation affected this dependency.

Keywords: surface topography; fretting; wear; coefficient of friction

1. Introduction

Fretting is the motion between two contacting parts when the sliding amplitude is small. When the amplitude of oscillation is larger than the radius of elastic contact, reciprocating sliding occurs [1]. Depending on the normal load, the following regimes can be recognized when the sliding amplitude increases: stick, partial slip and gross slip [2–4]. Varenberg et al. [5,6] introduced the slip index, which is a criterion to define various fretting regimes. For a low displacement amplitude, a partial slip occurs. When the sliding amplitude is higher, but smaller than a Hertzian contact radius, a gross slip takes place [7]. Fretting regimes are related to the kinds of damage; a material loss occurs in a gross slip, but cracking occurs in a partial slip. Various types of wear occur during fretting: abrasion, adhesion, oxidation and surface fatigue [8].

In fretting, wear oxide debris is formed. Wear particles can have two contrary influences on wear loss; beneficial or harmful [9,10]. Varenberg et al. [8] found that wear debris for dominant adhesion diminished, while for prevailing abrasion, it simplified material loss. Wear debris is also related to the coefficient of friction [11]. Diomidis and Mischler [12] found that an increase in the stroke caused increases in the sizes of wear particles when the fretting stroke increased. During fretting of steel elements, the created wear particles are non-cohesive and loose; therefore, they can be removed without difficulty [13].

Many variables (about 50) affect fretting wear [14,15]; a stroke, a normal force, a frequency and surface hardness seem to be the most important.

Fretting wear is proportional to the stroke [16,17]. It was found that when the amplitude of displacement increased, the friction coefficient also increased. Decreasing the normal load reduced the volumetric wear. However, increasing the contact pressure reduced the sliding amplitude, leading to operating in the partial slip regime [18]. Kalin et al. [19] performed dry fretting tests with silicon carbide against bearing steel counterparts. The wear volume increased exponentially with the amplitude.
However, in research reported in [12], the coefficient of friction showed no dependence on the amplitude of oscillation, and only the wear rate increased with the stroke.

Several researchers studied the impact of frequency on fretting. When the frequency of oscillation (0.01–60 Hz) was higher, the fretting damage of steel samples was lower [20]. However, Soderberg et al. [21] found that the fretting wear of steel samples was also marginally affected by the frequency (between 10 and 10,000 Hz). Odell and Vingsbo [22] found that the amplitude at the transition between gross and partial slips decreased when the frequency was smaller than 300 Hz. Li et al. [23] analyzed the influence of the frequency (1–80 Hz) on the contact of steel samples under fretting conditions. They considered changes in accumulated dissipated energy, which is proportional to the wear volume [7,24]. A decrease in this energy and a growth in the maximum coefficient of friction were observed with increasing frequency [23]. Park et al. [25,26] found that an increase in the frequency led to higher wear for contacts between tin-plated and tin-coated brass. The fretting wear of sintered iron was studied by the authors of [27]. Higher frictional resistance corresponded to higher frequency, while the wear level changed in the opposite direction. The fretting wear performance of two magnesium alloys was investigated [28]. The volumetric wear increased with increasing normal load and decreased with increasing frequency; however, the frequency had a marginal effect on the friction coefficient.

The relationship between hardness of co-acting parts and fretting wear was found to be complex. Kayaba and Iwabuchi [29] found that wear of harder steel was higher than that of a softer one, thanks to protection of the harder sample by oxide wear debris. The effect of the hardness of structural steel on wear of the sliding pair—structural steel–bearing steel—was negligible [30]. Budinsky [30] conducted fretting experiments with hard steel against steels of varying hardness. Fretting wear increased when the difference in hardness levels between two counterparts was large. Lemm et al. [15], in contrast to [29–31], used the same steel for both counterparts, in which the hardness was varied. For significantly different levels of hardness between two samples, the wear of the harder specimen was larger than that of the softer one. Oxide-based abrasive particles were observed to be embedded into the softer specimen, leading to its protection to wear. A similar effect was observed in tests in which a hard steel contacted a softer aluminum alloy [32,33].

The surface topography of sliding parts probably has a substantial effect on wear particle occurrence in the contact zone because these particles can escape to neighboring valleys when the surface is rough. Therefore increasing the surface roughness height seems to be a method of improving fretting wear resistance [8,34]. However, different effects of the surface texture on fretting have been previously achieved. Kubiak et al. [35,36] achieved a lower friction force for rougher discs. On the contrary, Pawlus et al. [37] found that for a lower roughness height of the disc sample, the total wear of the tribological system and the coefficient of friction were also lower. Yoon et al. [38] studied the effect of ball surface roughness on fretting. Lower friction coefficients in an initial part of the test were observed for the polished (smoother) sphere than for the non-polished (rougher) sphere. The dissipated energy behaved similar to the maximum coefficient of friction. Li et al. [23] found that the accumulated dissipated energy for a sliding pair with a laser-polished sphere was larger than that for the non-polished sphere. Raeymaekers and Talke [18] observed that the total dissipated energy was marginally higher for the laser-polished sphere than for the regular hemisphere. The authors of [39] found that differences in the surface texture affected the fretting wear between two Zn–Ni coatings. Rougher coatings had much deeper wear scars and more oxidized wear debris than smoother coatings. In [40], the fretting wear of Al–Si alloys after various surface preparations was studied. An increase in the surface roughness height led to improved wear resistance. The authors of [41] investigated the influence of the surface texture of steel discs contacting ceramic balls on the tribological performance of the sliding assembly in a dry gross sliding fretting regime and found that the results were better for lower disc roughness heights. The influence of disc surface texturing on dry gross sliding fretting of a ball-on-disc assembly was investigated [42]. The effect of surface texturing depended on the dominant wear type (adhesion or abrasion). Surface roughness affected the friction coefficient at the transition
between partial and gross slips; for lower heights, this coefficient was higher [43,44]. Leonard et al. [45] modelled fretting wear using the combined finite-discrete element method. A rougher surface led to higher wear. However, the role of the initial surface roughness in the gross slip regime seems to be important only at the beginning of tests.

One can see from this review that the effect of the surface topography of contacting elements on the tribological performances of sliding pairs in gross sliding fretting regimes is still unclear.

2. Materials and Methods

Tests were conducted using an Optimol SRV5 tribological tester (Optimol Instruments Prüftechnik GmbH, Munich, Germany) in a flat-on-ball configuration. The previous versions of this tester were used in other fretting experiments [16,18,36]. Balls of 5 mm radius R slid against discs in a dry gross sliding fretting regime (fulfilling the criteria contained in [1,4,5]). Balls and discs were made from 100Cr6 steel, of equal hardness (60 HRC). Experiments were conducted at a temperature of 30 °C, at 25–35% relative humidity. The number of cycles (18,000) was constant. Table 1 presents the experimental conditions. Before each test, samples were cleaned in acetone. The minimum number of test repetitions was three.

Table 1. Experimental conditions of gross sliding fretting tests.

| Test Designation | Stroke s, mm | Frequency f, Hz | Normal load P, N |
|------------------|-------------|----------------|-----------------|
| A                | 0.2         | 20             | 45              |
| B                | 0.15        | 20             | 45              |
| C                | 0.1         | 20             | 45              |
| D                | 0.1         | 20             | 15              |
| E                | 0.1         | 50             | 15              |
| F                | 0.1         | 50             | 45              |

Surface topographies of machined and worn counterparts were measured by a Talysurf CCI Lite scanning coherent interferometer (Taylor Hobson, Leicester, UK). The measured areas were 3.3 × 3.3 mm², and sampling intervals in perpendicular directions were 3.2 μm. The average value of the Ra parameter of machined balls was 0.15 μm. Discs were prepared by various methods including polishing (P), lapping (L), milling (M), grinding (G) and vapour blasting (VB). Tribological tests of anisotropic disc topographies (M and G) were conducted perpendicularly to lays (main directions). The wear volume $V_{\text{tot}}$ of the whole tribological system was computed as Equations (1)–(3):

$$V_{\text{tot}} = V_{\text{disc}} + V_{\text{ball}}.$$  
(1)

$$V_{\text{disc}} = (V_{\text{disc}}-) - (V_{\text{disc}}+),$$  
(2)

$$V_{\text{ball}} = (V_{\text{ball}}-) - (V_{\text{ball}}+),$$  
(3)

where volumes $(V_{\text{disc}}+)$ and $(V_{\text{ball}}+)$ were buildups or materials transferred; volumes $(V_{\text{disc}}-)$ and $(V_{\text{ball}}-)$ were lost materials [13,32].

The wear levels of discs were assessed only after surface leveling, and a digital filtration was not used. Before the calculation of wear levels of the balls, their curvatures were eliminated using spheres.

Table 2 shows selected surface topography parameters of discs before wear: the root mean square height $S_q$, the texture aspect ratio $S_t$, the autocorrelation length $S_a$, the skewness $S_s$, the kurtosis $S_k$ and the root mean square slope $S_d$ [46]. Figure 1 shows contour maps of the disc surfaces.
Table 2. Parameters of surface topographies of discs: Sq, Ssk, Sku, Sal, Str and Sdq before fretting tests.

| Surface | Sq, µm | Ssk | Sku | Sal, mm | Str    | Sdq   |
|---------|--------|-----|-----|---------|--------|-------|
| VB1     | 2.65   | −0.5| 4.6 | 0.026   | 0.872  | 0.478 |
| VB2     | 1.13   | −0.9| 6.6 | 0.021   | 0.851  | 0.193 |
| M1      | 0.95   | −0.25| 2.7 | 0.07    | 0.205  | 0.085 |
| M2      | 0.66   | −0.5| 3.86| 0.034   | 0.118  | 0.075 |
| G1      | 0.5    | −0.7| 5.5 | 0.019   | 0.036  | 0.118 |
| G2      | 0.37   | −0.56| 3.96| 0.023   | 0.046  | 0.075 |
| P       | 0.03   | −0.8| 7.1 | 0.0465  | 0.448  | 0.0082|
| L       | 0.31   | −0.57| 2.9 | 0.02    | 0.0154 | 0.0742|

Figure 1. Contour maps of disc surfaces: after vapour blasting VB1 and VB2, after milling M1 and M2, after grinding G1 and G2, after polishing P and after lapping L.

The heights (Sq) and slopes (Sdq) of isotropic (the Str parameter in the range: 0.85–0.87) vapour-blasted surfaces VB1 and VB2 were the biggest. The surface height of the sample VB2 after finish vapour blasting was smaller. Anisotropic samples after finish milling M1 and M2 had radial structures, but after grinding G1 and G2, they had one-directional structures. Amongst the anisotropic surfaces, the M1 sample was the roughest and had the largest autocorrelation length Sal. The height of the finish ground surface G2 was smaller than that of the rough ground G1 texture. The heights of the milled M2 and ground G1 samples G1 were similar. The correlation lengths of samples after finish milling were larger than those of discs after grinding. The roughness heights of polished P and
lapped L samples were the lowest. The surfaces after milling had deterministic characters, while other surfaces had random characters.

The surfaces of worn counterparts were examined by scanning electron microscope (SEM) fitted out with an energy dispersive spectrometry (EDS) analyser.

3. Results and Discussion

Table 3 lists the results of the fretting tests. It shows the volumetric wear levels of discs and balls, and the mean and final coefficients of friction. There were 18,000 cycles, corresponding to a test duration of 15 min for the frequency of 20 Hz, and 6 min for the frequency of 50 Hz. When the frequency was 20 Hz, the average value of the largest friction coefficient (COF$_{50-900}$) was estimated after removal of the early parts of the results (rapid growths of the coefficient of friction) before 50 s of the test, while the final value (COF$_{500-900}$) was assessed as the mean from the last five minutes of the test. When the frequency was set to 50 Hz, COF$_{50-360}$ characterized the mean and COF$_{300-360}$ characterized the final friction coefficient.

| Test Designation | Disc Surface | V$_{ball}$, $\mu m^3$ | V$_{ball}$, $\mu m^3$ | V$_{disc}$, $\mu m^3$ | V$_{disc}$, $\mu m^3$ | V$_{ball}$, $\mu m^3$ | V$_{ball}$, $\mu m^3$ | $V_{total}$, $\mu m^3$ | COF$_{50-900}$ | COF$_{500-900}$ |
|------------------|--------------|-----------------------|-----------------------|-----------------------|-----------------------|-----------------------|-----------------------|-----------------------|----------------|----------------|
| A s = 0.2 mm f = 20 Hz P = 45 N | VB1 5,751,187 192,796 4,735,133 7436 5,558,391 4,727,697 10,286,088 0.89 0.92 | VB2 1,761,967 344,568 5,099,394 8994 1,417,299 5,090,500 6,507,899 0.9 0.95 | M1 2,543,358 144,203 4,518,717 17,577 2,399,155 4,501,140 6,900,295 0.89 0.94 | M2 958,319 937,410 5,350,101 5519 20,909 5,344,582 5,365,491 0.89 0.94 | G1 2,299,195 211,401 4,588,955 31,448 2,087,794 4,557,507 6,645,301 0.88 0.93 | G2 1,686,781 327,076 4,675,078 17,311 1,359,705 4,657,767 6,017,472 0.89 0.93 | P 1,089,701 364,045 3,669,498 973 725,656 3,668,525 4,394,181 0.85 0.92 | L 1,219,342 403,471 4,459,393 8994 815,871 4,450,499 5,266,370 0.9 0.95 |
| B s = 0.15 mm f = 20 Hz P = 45 N | VB1 3,258,026 93,397 2,890,038 7436 3,164,629 2,882,602 6,047,231 0.9 0.93 | VB2 1,484,837 1,049,037 4,043,784 8137 435,800 4,035,647 4,471,447 0.88 0.95 | M1 1,140,223 80,164 3,808,204 29,495 1,060,059 3,778,709 4,838,768 0.96 1.02 | M2 750,209 1,151,923 4,421,414 4302 401,714 4,417,112 4,015,398 0.91 0.98 | G1 846,395 550,909 3,590,759 32,553 295,486 3,558,206 3,853,692 0.89 0.95 | G2 1,181,852 18,356 3,760,894 11,346 1,163,496 3,749,548 4,913,044 0.96 1 | P 1,333,566 119,097 2,725,342 14 1,214,469 2,725,328 3,939,797 0.96 1.02 | L 854,582 359,220 3,660,324 10,598 495,362 3,669,746 4,145,088 0.86 0.93 |
| C s = 0.1 mm f = 20 Hz P = 45 N | VB1 1,245,437 384,503 2,217,610 28,833 860,934 2,188,777 3,049,711 0.96 1 | VB2 1,050,962 67,675 1,373,249 37,254 983,287 1,335,995 2,319,282 0.94 1 | M1 707,693 65,643 1,701,742 16,530 642,050 1,685,212 2,327,262 0.93 1.01 | M2 519,194 424,163 2,438,983 9360 77,031 2,429,623 2,506,654 0.92 0.98 | G1 518,063 367,950 2,218,546 37,754 150,113 2,180,792 2,330,905 0.91 0.97 | G2 340,822 419,387 1,969,885 12,898 78,565 1,956,987 1,878,422 0.94 1 | P 201,539 916,405 2,393,498 227 714,866 2,393,271 1,678,405 0.93 1 | L 465,848 239,594 2,129,954 19,625 226,254 2,110,329 2,336,583 0.92 0.98 |
| D s = 0.1 mm f = 20 Hz P = 15 N | VB1 2,854,881 11,649 785,083 431,423 2,843,232 353,660 3,196,892 1.12 1.13 | VB2 1,179,948 21,418 1,047,159 117,925 1,158,530 929,234 2,087,764 1.08 1.12 | M1 1,508,291 26,515 1,317,243 20,301 1,481,776 1,296,942 2,775,718 1.1 1.13 | M2 1,011,996 12,048 881,287 17,653 999,948 863,634 1,863,582 1.06 1.09 | G1 1,326,692 12,452 814,496 46,223 1,314,240 768,273 2,082,513 1.1 1.15 | G2 654,536 20,406 1,034,300 14,157 634,130 1,020,143 1,654,273 1.09 1.12 | P 426,287 25,047 987,545 1284 401,240 986,261 1,387,501 1.13 1.15 | L 906,603 44,715 1,119,316 812 861,888 1,118,504 1,980,392 1.09 1.12 |
The maximum surface elastic contact pressure $p_0$ was calculated by Equation (4) [47]:

$$p_0 = \left( \frac{6PE^2}{\pi^3R^2} \right)^{\frac{1}{3}}. \quad (4)$$

The radius of elastic contact length $a$ was computed by the following Equations (5) and (6) [47]:

$$a = \left( \frac{3PR}{4E^*} \right)^{\frac{1}{3}}. \quad (5)$$

where:

$$E^* = \left( \frac{1 - \nu_1^2}{E_1} + \frac{1 - \nu_2^2}{E_2} \right)^{-1} \quad (6)$$

$E_{1,2} = $ Young’s moduli, $\nu_{1,2} = $ Poisson’s ratios.

When the normal force was 45 N, the Hertzian radius of contact $a$ was 0.114 mm; it was higher than the largest amplitude of oscillation (0.1 mm), and therefore fretting occurred. In this case, the maximum elastic contact pressure $p_0$ was 1652 MPa.

The variation of the friction coefficient was typically not higher than 0.03. Scatters of total volumetric wear were usually not higher than 14% for assemblies with the same disc samples. Table 3 lists the results of experimental investigations.

In test A, the wear of the discs was typically higher than the wear of the balls, but the sliding pair with the roughest disc sample VB1 was the exception. The final friction coefficient COF$_{50-900}$ was similar for various assemblies; however, the average friction coefficient COF$_{50-900}$ was the smallest for the sliding pair containing the polished disc P of the lowest roughness height. The friction coefficient initially increased and then obtained a stable value typically after 15,000 cycles (Figure 2a). The total volumetric wear level was proportional to the disc surface height determined by the Sq parameter; the coefficient of linear correlation was 0.95 (Figure 3a).

### Table 3. Cont.

| Test Designation | Disc Surface | $V_{ball}$, $\mu$m$^3$ | $V_{ball}$, $\mu$m$^3$ | $V_{disc}$, $\mu$m$^3$ | $V_{disc}$, $\mu$m$^3$ | $V_{ball}$, $\mu$m$^3$ | $V_{ball}$, $\mu$m$^3$ | COF$_{50-360}$ | COF$_{300-900}$ |
|------------------|--------------|------------------------|------------------------|------------------------|------------------------|------------------------|------------------------|----------------|----------------|
| **E** s = 0.1 mm f = 50 Hz P = 15 N | VB1 | 3,227,445 | 33,450 | 285,173 | 865,175 | 3,193,995 | -580,002 | 2,613,993 | 1.12 | 1.13 |
| | VB2 | 805,101 | 7064 | 917,141 | 2819 | 798,037 | 941,322 | 1,712,359 | 1.14 | 1.16 |
| | M1 | 642,892 | 19,212 | 941,479 | 1882 | 623,680 | 939,597 | 1,563,277 | 1.11 | 1.16 |
| | M2 | 176,842 | 1,112,931 | 2819 | 798,037 | 941,322 | 1,712,359 | 1.11 | 1.16 |
| | G1 | 291,999 | 19,212 | 941,479 | 1882 | 623,680 | 939,597 | 1,563,277 | 1.14 | 1.16 |
| | P | 273,365 | 131,520 | 953,358 | 11,421 | 141,845 | 942,137 | 1,083,982 | 1.16 | 1.21 |
| **F** s = 0.1 mm f = 50 Hz P = 45 N | VB1 | 3,221,366 | 17,892 | 1,657,568 | 576,659 | 3,203,474 | 1,080,909 | 4,284,383 | 0.85 | 0.94 |
| | VB2 | 368,583 | 632,212 | 2,487,315 | 67,377 | 368,229 | 2,419,938 | 2,156,309 | 0.92 | 1.07 |
| | M1 | 421,753 | 638,573 | 2,470,523 | 44,431 | 375,706 | 2,426,092 | 2,209,272 | 0.89 | 1.02 |
| | M2 | 1,148,666 | 1,334,720 | 2,830,504 | 3717 | 1,228,301 | 2,826,938 | 2,100,481 | 0.96 | 1.07 |
| | G1 | 591,749 | 604,496 | 2,184,448 | 19,451 | 512,937 | 2,164,997 | 2,152,272 | 0.9 | 1.03 |
| | G2 | 187,920 | 835,974 | 2,420,636 | 648,054 | 1,768,794 | 2,416,848 | 1,768,794 | 0.91 | 1.05 |
| | P | 86,437 | 875,835 | 2,376,765 | 578 | 789,398 | 2,376,187 | 1,586,789 | 0.93 | 1.0 |
| | L | 475,883 | 415,024 | 2,366,206 | 650 | 60,859 | 2,365,556 | 2,426,415 | 0.895 | 1.0 |

The maximum surface elastic contact pressure $p_0$ was calculated by Equation (4) [47]:

$$p_0 = \left( \frac{6PE^2}{\pi^3R^2} \right)^{\frac{1}{3}}. \quad (4)$$

The radius of elastic contact length $a$ was computed by the following Equations (5) and (6) [47]:

$$a = \left( \frac{3PR}{4E^*} \right)^{\frac{1}{3}}. \quad (5)$$

where:

$$E^* = \left( \frac{1 - \nu_1^2}{E_1} + \frac{1 - \nu_2^2}{E_2} \right)^{-1} \quad (6)$$

$E_{1,2} = $ Young’s moduli, $\nu_{1,2} = $ Poisson’s ratios.
Materials containing all selected discs. The shapes of the presented curves are similar to those obtained in tests the average friction coefficient COF50-900. The final values of the coefficient of friction COF 600-900 were topography heights (Figure 5b). The roughest disc sample VB1 led to the highest total wear level and the discs. Similar to the assemblies analysed, the previous wear of the system was proportional to the disc roughness height (Figure 5a). The average coefficients of friction were higher for bigger disc to 0.1 mm led to smaller volumetric wear without a change in the final coefficient of friction.

A reduction in the stroke from 0.15 (test B) than the largest amplitude of oscillation (0.1 mm), and therefore fretting occurred. In this case, the maximum elastic contact pressure was 1652 MPa. When the normal force was 45 N, the Hertzian radius of contact \( E = \frac{1}{1-\nu} \) computed by the following Equations (5) and (6) [47]:

\[
\begin{align*}
E &= \frac{1}{1-\nu} \\
p_0 &= 6PE^2/\lambda
\end{align*}
\]

\( p_0 \) was calculated by the following Equation (4) for selected assemblies with discs: after vapour blasting VB1, after lapping L and after milling M2.

\[
\begin{align*}
\mu &= \frac{1}{1-v_1} - \frac{1}{1-v_2} - \frac{1-v_1}{1-v_2} (1-v_2)\
\end{align*}
\]

The variation of the friction coefficient was typically not higher than 0.03. Scatters of total volumetric wear of tribological system \( V_{total} \), \( COF_{total} \) during tests A; \( s = 0.2 \, \text{mm}, P = 45 \, \text{N}, f = 20 \, \text{Hz} \) (a) and during test B; \( s = 0.15 \, \text{mm}, P = 45 \, \text{N}, f = 20 \, \text{Hz} \) (b) for selected assemblies with discs: after vapour blasting VB1, after lapping L and after milling M2.

In test A, the wear of the discs was typically higher than the wear of the balls, but the sliding contact of the ball. For different sliding pairs, the opposed situation was observed. The wear of the balls was inversely proportional to the wear of the discs. Similarly to test A, the friction coefficient after initial runs of the maximum coefficients of friction during tests C for sliding pairs L, were initially increased and then obtained a stable value typically after 15,000 cycles (Figure 2a). The total wear of the sliding pair containing the polished disc P of the lowest roughness height. The friction coefficient after initial runs of the maximum coefficients of friction during tests C for sliding pairs L, were initially increased and then obtained a stable value typically after 15,000 cycles (Figure 2a). The total wear of the sliding pair containing the disc after lapping L and after milling M2.

In test B, for the sliding pair containing disc VB 1, the wear rate of the disc was lower than that of the ball. For different sliding pairs, the opposed situation was observed. The wear of the balls was inversely proportional to the wear of the discs. Similarly to test A, the friction coefficient after initial runs of the maximum coefficients of friction during tests C for sliding pairs L, were initially increased and then obtained a stable value typically after 15,000 cycles (Figure 2a). The total wear of the sliding pair containing the disc after lapping L and after milling M2.

The maximum surface elastic contact pressure \( po \) was calculated by the following Equation (4):

\[
po = 6P(E^2/\lambda)
\]

The radius of elastic contact length \( a \) was computed by the following Equations (5) and (6) [47]:

\[
\begin{align*}
a &= \frac{3PR}{E} \\
p_0 &= \frac{6P}{\lambda}
\end{align*}
\]

\( a \) was computed by the following Equations (5) and (6) [47]:

\[
\begin{align*}
E &= \frac{1}{1-\nu} \\
p_0 &= 6PE^2/\lambda
\end{align*}
\]

The coefficient of linear correlation was 0.95 (Figure 3a). The variation of the friction coefficient was typically not higher than 0.03. Scatters of total volumetric wear of tribological system \( V_{total} \), \( COF_{total} \) during tests A; \( s = 0.2 \, \text{mm}, P = 45 \, \text{N}, f = 20 \, \text{Hz} \) (a) and during test B; \( s = 0.15 \, \text{mm}, P = 45 \, \text{N}, f = 20 \, \text{Hz} \) (b).
In test B, for the sliding pair containing disc VB1, the wear rate of the disc was lower than that of the ball. For different sliding pairs, the opposed situation was observed. The wear of the balls was inversely proportional to the wear of the discs. Similarly to test A, the friction coefficient after initial sharp growth, increased slowly and obtained a stable value in most cases after 15,000 cycles (Figure 2b). The smallest friction coefficient was achieved for the assembly containing the disc after lapping L, while the highest coefficient was achieved for sliding pairs with discs after polishing P, milling M1, and grinding G2. A decrease in the amplitude of oscillation from 0.1 (test A) to 0.075 mm caused a reduction in volumetric wear, but had a marginal effect on the coefficient of friction. Total wear was proportional to the standard deviation of the disc height; the linear coefficient of correlation was 0.85 (Figure 3b).

Figure 4 shows the runs of the maximum coefficients of friction during tests C for sliding pairs containing all selected discs. The shapes of the presented curves are similar to those obtained in tests A and B. In all analysed cases, the wear levels of the balls were much lower than the wear levels of the discs. Similar to the assemblies analysed, the previous wear of the system was proportional to the disc roughness height (Figure 5a). The average coefficients of friction were higher for bigger disc topography heights (Figure 5b). The roughest disc sample VB1 led to the highest total wear level and the average friction coefficient COF$_{50-900}$ was similar for various sliding pairs (between 0.97 and 1.01). A reduction in the stroke from 0.15 (test B) to 0.1 mm led to smaller volumetric wear without a change in the final coefficient of friction.

![Figure 4](image-url)  
**Figure 4.** Maximum coefficient of friction during test C for assemblies with all (a) and selected discs after vapour blasting VB1, after lapping L and after milling M2 (b) for the following operating parameters: $s = 0.1$ mm, $P = 45$ N, $f = 20$ Hz.

In test D, contrary to the results analysed previously, the average wear rates of the balls were similar to those of the discs. The assembly with the roughest disc VB1 led to the biggest, while the smoothest disc P, led to the smallest wear volume of the tribological system. The wear of the balls and the total wear were proportional to the disc roughness height. The highest coefficient of friction was obtained for the roughest sample VB1, while the smallest was obtained for sample M2 after milling. The friction forces increased during tests and obtained steady values typically after 9000 cycles (Figure 6a). A reduction in the contact pressure for the same frequency of oscillations (test C) caused a slight wear decrease and growth in the friction coefficient.
Figure 4. Maximum coefficient of friction during test C for assemblies with all (a) and selected discs (b) after vapour blasting VB1, after lapping L and after milling M2 for the following operating parameters: \( s = 0.1 \text{ mm} \), \( P = 45 \text{ N} \), \( f = 20 \text{ Hz} \).

Figure 5. Dependencies between disc surface height determined by the Sq parameter and total volumetric wear of system \( V_{\text{total}} \) (a) and the mean coefficient of friction (b) in test C: \( s = 0.1 \text{ mm} \), \( P = 45 \text{ N} \), \( f = 20 \text{ Hz} \).

In test E, the wear of the balls was typically lower than the wear of the discs, but assemblies with VB1 and G1 discs were the exceptions. Similar to other tests, the volumetric wear was proportional to the disc roughness height. The total wear of the sliding pair with the roughest disc sample VB1 was the biggest, but with the smoothest disc P, it was the lowest. The wear of the balls was inversely related to the wear of the discs. The highest mean friction coefficient was obtained for the sliding pair with the polished sample of the smallest height P, while the smallest was obtained for the assemblies with ground samples G1 and G2. It is interesting that the M2 sample after milling led to comparatively high frictional resistance, contrary to test D carried out at the same load and smaller frequency of oscillation. Similar to test D, the friction coefficient after early fluctuations typically obtained stable values after 9000 cycles (Figure 6b). A growth in the frequency of oscillations for the same load of 15 N (test D) caused wear reduction and growth in the friction coefficient.
In test D, contrary to the results analysed previously, the average wear rates of the balls were similar to those of the discs. The assembly with the roughest disc VB1 led to the biggest, while the smoothest disc P, led to the smallest wear volume of the tribological system. The wear of the balls and the total wear were proportional to the disc roughness height. The highest coefficient of friction was obtained for the roughest sample VB1, while the smallest was obtained for sample M2 after milling. The friction forces increased during tests and obtained steady values typically after 9000 cycles (Figure 6a). A reduction in the contact pressure for the same frequency of oscillations (test C) caused a slight wear decrease and growth in the friction coefficient.

Figure 6. Maximum coefficient of friction during test D; s = 0.1 mm, P = 15 N, f = 20 Hz; (a) and during test E; s = 0.1 mm, P = 15 N, f = 50 Hz (b) for selected assemblies with discs: after vapour blasting VB1, after lapping L and after milling M2.

In test E, the wear of the balls was typically lower than the wear of the discs, but assemblies with VB1 and G1 discs were the exceptions. Similar to other tests, the volumetric wear was proportional to the disc roughness height. The total wear of the sliding pair with the roughest disc sample VB1 was the biggest, but with the smoothest disc P, it was the lowest. The wear of the balls was inversely related to the wear of the discs. The highest mean friction coefficient was obtained for the sliding pair with the polished sample of the smallest height P, while the smallest was obtained for the assemblies with ground samples G1 and G2. It is interesting that the M2 sample after milling led to comparatively high frictional resistance, contrary to test D carried out at the same load and smaller frequency of oscillation. Similar to test D, the friction coefficient after initial fluctuations typically reached steady values as the test progressed. Figure 7 presents values of the maximum friction coefficient runs for sliding pairs with all and chosen discs in test F. The coefficient of friction after initial abrupt growth was stable between 2000 and 7000 cycles and then increased as the test progressed. The results presented in Figure 7b (the lowest friction coefficient of the assembly with VB1 disc) are different from those shown in Figure 4b obtained for the same normal load and smaller frequency of oscillations (test C). However, the change in the frequency for the same normal load caused a marginal change in total wear volume.
An increase in the normal load for the same frequency of oscillations (test E) led to wear growth and a reduction in the coefficient of friction.

Figure 7. Maximum coefficient of friction during test F for sliding pairs with all (a) and selected discs after vapour blasting VB1, after lapping L and after milling M2 (b) for the following operating parameters: \( s = 0.1 \text{ mm}, P = 45 \text{ N}, f = 50 \text{ Hz} \).

Figure 8 shows fretting loops for the sliding pair with a lapped L disc. One can observe changes in the relative displacements without changes in the coefficients of friction during the analysis of the fretting loops corresponding to tests A, B, C. After comparing fretting loops obtained after tests C and D, as well as F and E, it is evident that a reduction in the load led to growth in the friction coefficient and a change in the loop shape corresponding to a higher value of the slip index. An increase in the frequency from 20 (tests A, B, C and D) to 50 Hz (tests E and F) led to changes in fretting loop shapes (smaller stability of the coefficient of friction at a higher frequency).
Figure 8 shows fretting loops for the sliding pair with a lapped L disc. One can observe changes in the relative displacements without changes in the coefficients of friction during the analysis of the fretting loops corresponding to tests A, B, C. After comparing fretting loops obtained after tests C and D, as well as F and E, it is evident that a reduction in the load led to growth in the friction coefficient and a change in the loop shape corresponding to a higher value of the slip index. An increase in the frequency from 20 (tests A, B, C and D) to 50 Hz (tests E and F) led to changes in fretting loop shapes (smaller stability of the coefficient of friction at a higher frequency).

Figures 9 and 10 show contour maps of vapour-blasted VB1 and polished P discs and contacted balls, respectively, after various tests. It is evident that smaller volumetric wear occurred for the sliding pair containing the P disc compared to the VB1 disc. For assembly with VB1, the disc wear of the disc was typically lower than the wear of the ball, contrary to the assembly with the P disc. Wear of co-acting pairs had an abrasive-adhesive character. Plastic deformation also occurred on the vapour-blasted VB1 disc surface.
The disc was typically lower than the wear of the ball, contrary to the assembly with the P disc. Wear of co-acting pairs had an abrasive-adhesive character. Plastic deformation also occurred on the vapour-blasted VB1 disc surface.

Figure 9. Contour maps of disc vapour-blasted VB1 and contacted balls after tests: (A–F).
Figure 10. Contour maps of polished disc P and contacted balls after tests: (A–F).

The influence of the disc surface texture on the frictional resistance was evident mainly at the lowest amplitude of motion (0.05 mm), when wear of the disc was comparatively low. The effect of the disc surface texture on the friction coefficient depended on the frequency of oscillation. For the normal force of 45 N and the frequency of 20 Hz (test C), the highest disc roughness (VB1 sample) led to the
largest mean coefficient of friction; however, the opposed tendency occurred for the same load and the frequency of 50 Hz (test F). For the lower normal force of 15 N, a similar effect of frequency on friction force was not as apparent; however, in test E (frequency of 50 Hz), the highest mean friction coefficient was obtained for the assembly containing the disc P with the smallest height.

The total wear rate was proportional to the height of the disc surface, determined by the value of the Sq parameter, independently of the operating conditions. In tests A, C, D, E and F, the total wear of assembly with the roughest vapour-blasted VB1 sample was the highest, it was the smallest with the smoothest polished specimen P. This performance probably resulted from the fact that rougher surfaces, of higher plasticity indices [48,49], have a larger tendency to plastic deformation and hence wear. Tracks of the plastic deformation were found on the VB1 disc surface after tribological tests (Figure 9). The wear level of balls was typically smaller than of discs, but the assembly with the roughest VB1 disc was the exception.

Previously, experiments were conducted using the same tester [50]. Steel balls made of 100Cr6 steel of 60 HRC hardness contacted discs of various surface topographies made of 42CrMo4 steel of 40 HRC hardness under the same conditions as in the tests A, B, C. In the previous tests the resistance to motion was the smallest when the movement of the ball was orthogonal to the main direction of the finished milled disc surface. These results were probably related to formation of the layer of oxidized wear particles on the disc surface and the smaller wear of discs compared to the wear of balls. However, in the present tests, this effect disappeared. Oxidised abrasive particles were embedded into both counterparts (Figures 11 and 12). A low coefficient of friction of assembly with the milled disc surface M2 was achieved only in test D. An increase in hardness of the disc compared to the results presented in [50] led to a smaller role of the oxidized debris layer, and hence, smaller wear of the tribological system and typically smaller wear of the balls compared to that of discs. A decrease in total wear of a sliding pair due to a decrease in hardness differences was found in the other works [14,31].

![Figure 11. Energy dispersive spectrometry (EDS) analysis of worn lapped disc L after test A; s = 0.2 mm, P = 45 N, f = 20 Hz.](image)

| No. | O, %  | V, %  | Cr, %  | Fe, %  | Mo, %  | W, %  |
|-----|-------|-------|--------|--------|--------|-------|
| 1   | 3.44  | 2.98  | 4.33   | 73.41  | 5.02   | 7.18  |
| 2   | 31.83 | 1.12  | 2.40   | 54.31  | 2.30   | 3.17  |
| 3   | 31.21 | 0.85  | 2.35   | 55.95  | 2.46   | 3.10  |
| 4   | 30.74 | 1.11  | 2.36   | 56.03  | 2.31   | 3.06  |
| 5   | 28.06 | 4.04  | 2.84   | 48.35  | 5.61   | 7.21  |
| 6   | 30.82 | 1.05  | 2.25   | 56.99  | 2.23   | 2.83  |
| 7   | 25.03 | 2.09  | 3.26   | 57.81  | 3.26   | 4.12  |

A decrease in the stroke led to wear reduction. A reduction in the contact pressure led to growth in the friction coefficient and a reduction in the wear volume. An increase in the frequency of oscillation led to an increase in the coefficient of friction and a reduction in volumetric wear only when a lower normal force was applied (15 N). Similar results were obtained for different hardness of counterparts [51].
wear of the tribological system was proportional to the disc roughness height. The influence of the disc surface texture on the friction coefficient was substantial only for the smallest stroke of 0.1 mm. The frequency of oscillation had an effect on this dependence. For the normal load of 45 N and the frequency of 20 Hz, the highest disc roughness corresponded to the largest mean coefficient of friction; however, after increasing the frequency to 50 Hz, the biggest disc amplitude led to the smallest frictional resistance.

A reduction in the amplitude of oscillation decreased wear but had marginal influence on the coefficient of friction. The friction coefficient increased and total wear decreased due to a reduction in the normal load. When the frequency increased, wear decreased and the friction coefficient increased. These effects were visible only when a lower normal load was applied.

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**References**

1. Fouvry, S.; Kapsa, P.H.; Vincent, L. Analysis of sliding behavior for fretting loading: Determination of transition criteria. *Wear* **1995**, *185*, 21–46. [CrossRef]
2. Vingsbo, O.; Soerberg, S. On fretting maps. *Wear* **1988**, *126*, 131–147. [CrossRef]
3. Zhou, Z.R.; Nakazawa, S.; Zhu, M.H.; Maruyama, N.; Kapsa, P.H.; Vincent, L. Progress in fretting maps. *Tribol. Int.* **2006**, *39*, 1068–1073. [CrossRef]
4. Varenberg, M. Towards a unified classification of wear. *Friction* **2013**, *1*, 333–340. [CrossRef]
5. Varenberg, M.; Etsion, I.; Halperin, G. Slip index: A new unified approach to fretting. *Tribol. Lett.* **2004**, *17*, 569–573. [CrossRef]
6. Varenberg, M.; Etsion, I.; Altus, E. Theoretical substantiation of the slip index approach to fretting. *Tribol. Lett.* **2005**, *19*, 263–264. [CrossRef]
7. Fouvry, S.; Paulin, C.; Liskiewicz, T. Application of an energy wear approach to quantify fretting contact durability: Introduction of a wear energy capacity concept. *Tribol. Int.* **2007**, *40*, 1428–1440. [CrossRef]
8. Varenberg, M.; Halperin, G.; Etsion, I. Different aspects of the role of wear debris in fretting wear. *Wear* **2002**, *252*, 902–910. [CrossRef]
9. Ding, J.; McColl, I.R.; Leen, S.B.; Shipway, P.H. A finite element based approach to simulating the effects of debris on fretting wear. Wear 2007, 26, 481–491. [CrossRef]

10. Iwabuchi, A. The role of oxide particles in the fretting wear of mild steel. Wear 1991, 151, 337–344. [CrossRef]

11. Diomidis, N.; Mischler, S. Third body effects on friction and wear during fretting of steel contacts. Tribol. Int. 2011, 44, 1452–1460. [CrossRef]

12. Hu, Q.; McColl, I.R.; Harris, S.J.; Waterhouse, R.B. The role of debris in the fretting wear of a SiC reinforced aluminum alloy matrix composite. Wear 2000, 245, 10–21. [CrossRef]

13. Berthier, Y.; Vincent, L.; Godet, M. Fretting fatigue and fretting wear. Tribol. Int. 1989, 22, 235–242. [CrossRef]

14. Dobromirski, J. Variables of Fretting Process: Are There 50 of Them? ASTM International: West Conshohocken, PA, USA, 2009.

15. Lemm, J.D.; Warwuth, A.R.; Pearson, S.R.; Shipway, P.H. The influence of surface hardness on the fretting wear of steel pairs—Its role in debris retention in the contact. Tribol. Int. 2015, 81, 258–266. [CrossRef]

16. Ohnmae, N.; Tsukizoe, T. The effect of slip amplitude on fretting. Wear 1974, 27, 281–294. [CrossRef]

17. Li, J.; Lu, Y.H. Effects of displacement amplitude on fretting wear behaviors and mechanism of Inconel 600 alloy. Wear 2013, 304, 223–230. [CrossRef]

18. Raeymaekers, B.; Talke, F.E. The effect of laser polishing on fretting wear between a hemisphere and a flat plate. Wear 2010, 269, 416–423. [CrossRef]

19. Kalin, M.; Vizintin, J.; Novak, S. Effect of fretting conditions on the wear of silicon nitride against bearing steel. Mater. Sci. Eng. A 1996, A220, 191–199. [CrossRef]

20. Toth, L. The investigation of the steady stage of steel fretting. Wear 1972, 20, 277–286. [CrossRef]

21. Soderberg, S.; Bryggman, U.; McCullough, T. Frequency effects in fretting wear. Wear 1986, 110, 19–34. [CrossRef]

22. Odfalk, M.; Vingsbo, O. Influence of normal force and frequency on fretting. Tribol. Trans. 1990, 33, 604–610. [CrossRef]

23. Li, L.; Etsion, I.; Talke, F.E. The effect of frequency on fretting in a micro-spherical contact. Wear 2011, 270, 857–865. [CrossRef]

24. Fouvy, S.; Kapsa, P.; Zabouani, H.; Vincent, L. Wear analysis in fretting of hard coatings through a dissipated energy concept. Wear 1997, 203, 393–403. [CrossRef]

25. Park, Y.W.; Narayanan, T.S.; Lee, K.Y. Effect of fretting amplitude and frequency on the fretting corrosion behavior of thin plated contacts. Surf. Coat. Technol. 2006, 201, 2181–2192. [CrossRef]

26. Park, Y.W.; Bapu, G.R.; Lee, K.Y. Studies of tin coated brass contacts in fretting conditions under different loads and frequencies. Surf. Coat. Technol. 2007, 201, 7939–7951. [CrossRef]

27. Leheup, E.R.; Zhang, D.; Moon, J.R. Fretting wear of sintered iron under low normal pressure. Wear 1998, 221, 86–92. [CrossRef]

28. Huang, W.; Hou, B.; Pang, Y.; Zhood, Z. Fretting wear behavior of AZ91D and AM60B magnesium alloy. Wear 2006, 260, 1173–1178. [CrossRef]

29. Kayanba, T.; Iwabuchi, A. Effect of hardness of hardened steel and the action of oxides on fretting wear. Wear 1981, 66, 27–41. [CrossRef]

30. Ramesh, R.; Gnanamoorthy, R. Effect of hardness on fretting wear behavior of structural steel En 24, against bearing steel, En 31. Mater. Des. 2007, 28, 1447–1452. [CrossRef]

31. Budinsky, K.C. Effect of hardness differential on metal-to-metal fretting damage. Wear 2013, 301, 501–507. [CrossRef]

32. Elleuch, K.; Fouvy, S. Wear analysis of AlSi7Mg aluminum alloy under fretting. Wear 2002, 253, 662–672. [CrossRef]

33. Elleuch, K.; Fouvy, S. Experimental and modeling aspects of abrasive wear of an AlSi7Mg aluminum alloy under gross slip fretting conditions. Wear 2005, 258, 40–49. [CrossRef]

34. Fu, Y.; Wei, J.; Batchelor, A.W. Some considerations on the mitigation of fretting damage by the application of surface-modification technologies. J. Mater. Process. Technol. 2000, 99, 231–245. [CrossRef]

35. Kubiak, K.J.; Liskiewicz, T.E.; Mathia, T.G. Surface morphology in engineering applications: Influence of roughness on sliding and wear in dry fretting. Tribol. Int. 2011, 44, 1427–1432. [CrossRef]

36. Kubiak, K.J.; Bigerelle, M.; Mathia, T.G.; d’Hardivilliers, W. Roughness of interface in dry contact under fretting conditions. In Proceedings of the 13th International Conference on Metrology and Properties of Engineering Surfaces, Twickenham Stadium, UK, 12–15 April 2011; pp. 99–102.
37. Pawlus, P.; Michalczewski, R.; Lenart, A.; Dzierwa, A. The effect of random surface topography height on fretting in dry gross slip conditions. *Proc. Inst. Mech. Eng. Part J* 2014, 228, 1374–1391. [CrossRef]
38. Yoon, Y.; Etsion, I.; Talke, F.E. The evolution of fretting wear in a micro-spherical contact. *Wear* 2011, 270, 567–575. [CrossRef]
39. Lee, L.; Régis, E.; Descartes, S.; Chromik, R.R. Fretting wear behavior of Zn–Ni alloy coatings. *Wear* 2015, 330–331, 112–121. [CrossRef]
40. Cho, I.S.; Amanov, A.; Kwak, D.H.; Jeong, B.J.; Park, I.G. The influence of surface modification techniques on fretting wear of Al–Si alloy prepared by gravity die casting. *Mater. Design* 2015, 65, 401–409. [CrossRef]
41. Lenart, A.; Pawlus, P.; Dzierwa, A. The effect of steel disc surface texture in contact with ceramic ball on friction and wear in dry fretting. *Surf. Topogr. Metrol. Prop.* 2018, 6, 034004. [CrossRef]
42. Lenart, A.; Pawlus, P.; Wos, S.; Dzierwa, A. The effect of surface texturing on dry gross fretting. *Lubricants* 2018, 6, 92. [CrossRef]
43. Kubiak, K.J.; Mathia, T.G.; Fouvry, S. Interface roughness effect on friction map under fretting contact conditions. *Tribol. Int.* 2010, 43, 1500–1507. [CrossRef]
44. Kubiak, K.J.; Mathia, T.G. Influence of roughness on contact interface in fretting under dry or lubricated sliding regimes. *Wear* 2009, 267, 315–321. [CrossRef]
45. Leonard, B.D.; Sadeghi, F.; Shindle, S.; Mittelbach, M. Rough surface and damage mechanics under wear modeling using the combined finite-discrete element method. *Wear* 2013, 305, 312–321. [CrossRef]
46. Leach, R. *Characterisation of Areal Surface Texture*; Springer: Berlin/Heidelberg, Germany, 2013.
47. Johnson, K.L. *Contact Mechanics*; Cambridge University Press: London, UK, 1985.
48. Greenwood, J.A.; Williamson, J.B.P. Contact of nominally flat surfaces. *Proc. R. Soc. (Lond.)* 1966, A295, 300–319.
49. Pawlus, P.; Zelasko, W. The importance of sampling intervals in contact mechanics. *Wear* 2012, 276, 121–129. [CrossRef]
50. Lenart, A.; Pawlus, P.; Dzierwa, A.; Sep, J.; Dudek, K. The effect of surface topography on dry fretting in the gross slip regime. *Arch. Civ. Mech. Eng.* 2017, 17, 894–904. [CrossRef]
51. Lenart, A.; Pawlus, P.; Dzierwa, A.; Tupaj, M. The effect of surface texture of steel disc on friction and fretting wear. *Tribologia* 2018, 280, 39–48. [CrossRef]

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