Research on Influence of Exhaust Characteristics and Control Strategy to DOC-Assisted Active Regeneration of DPF

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Abstract: For the purpose of designing a reasonable control strategy for DOC-assisted DPF regeneration, a mathematical model that describes the thermal phenomenon both in a diesel oxidation catalyst (DOC) and diesel particulate filter (DPF) during regeneration is developed. All boundary conditions of this model are obtained by experiments. The effects of the main exhaust parameters such as exhaust mass flow rate, exhaust temperature, oxygen concentration and emission of reactants are investigated comprehensively. The effects of two main parameters of control strategy, DOC-out temperature and soot loading, are analyzed as well. To quantify the effects of relevant parameters, the fuzzy grey relational analysis method is utilized to evaluate the correlation coefficient of all factors to key indexes of DPF regeneration such as maximum temperature, maximum rate of temperature increase and regeneration duration. The results of this work will greatly reduce the complexity of analysis and enable more rational control strategy design of DOC–DPF regeneration systems.

Keywords: DOC-assisted DPF regeneration; mathematical model; exhaust parameters; control strategy; fuzzy grey relational analysis

1. Introduction

With more and more stringent emission regulations of vehicles, the particulate emissions of diesel engines has raised a huge challenge for engine manufacturers and automotive engineers [1,2]. Great efforts have been made in the field of improving engine structure and combustion mode, such as high-pressure common rail injection system [3,4], HCCI (Homogeneous Charge Compression Ignition) [5–7], etc. [8–10], to reduce particle emission. Among all the technologies, the diesel particulate filter (DPF) is acknowledged to be the most effective device to reduce particulate emission [11,12]. Further, regeneration [13,14] is the key technique that determines the application and promotion of DPF.

Various regeneration methods have been implemented, such as post injection, microwave heating and continuous regeneration technology [15]. However, post injection in the cylinder causes engine performance deterioration and lubrication oil dilution [16]. Microwave heating is superior for its instantaneous penetration and selective absorption. Nevertheless, it is restricted by vehicle power supply and the complexity added to the electric control unit (ECU) [17]. Continuous regeneration technology (CRT) enables soot combustion at a relatively lower temperature, typically 250 °C. However, the catalyst used in a CRT system loses efficacy easily due to the high sulfur content in diesel oil, a process named catalyst poisoning [18]. At present, thermal regeneration of DPF assisted by a diesel oxidation catalyst (DOC) is widely used for its simplicity and reliability [19]. The working process of a DOC–DPF active regeneration system is shown in Figure 1. Firstly, after the regeneration is triggered, some amount of hydrocarbon (normally diesel fuel) is injected into the exhaust pipe, vaporizing and being oxidized in DOC along with those existing reactants in exhaust gas such as carbon monoxide, hydrocarbon and nitric oxides. Then,
the outlet temperature of DOC rises to a pre-set target temperature (DOC-out temperature), which is normally 600 °C. Finally, soot deposited in the DPF starts to burn until the regeneration is accomplished [20]. There are numerous investigations regarding DOC–DPF active regeneration. However, there are rarely studies concerning the influences of exhaust characteristics and control strategy parameters to regeneration.

![Figure 1. Working principle of a DOC–DPF system.](image)

The majority of studies focus on the influence of geometrical parameters of DPF and fuel types on active regeneration. Koji Tsuneyoshi and Kazuhiro Yamamoto [21,22] compared the performance of square and hexagonal cells in terms of filtration, pressure drop and regeneration on test bench. Deng et al. [23] investigated the influence of diameter, length, wall thickness and cell diameter on continuous regeneration of DPF with the improved fuzzy grey relational analysis method and found the most relevant factor to properties in equilibrium state. José Rodríguez-Fernández et al. [24] investigated the effect of alternative fuels on soot reactivity and implications for DPF regeneration. These scholars left out the operational parameters (namely exhaust characteristics and control strategy parameters), which is a research gap that deserves special attention.

Additionally, many theoretical models of DOC-DPF have been built to analyze regeneration properties. Björn Lundberg [25] developed a kinetic and transport model of DOC to capture transient features for typical lean exhaust conditions. Chaitanya S. Sampara [26] determined global kinetics for the oxidation of diesel fuel, propylene, carbon monoxide, hydrogen and nitrogen monoxide. Tae Joong Wang and Seung Wook Baek [27] also estimated kinetic parameters of a diesel oxidation catalyst under actual vehicle operating conditions. Christopher Depcik and Dennis Assanis [28] built a one-dimensional model of DOC to illustrate the physical and chemical phenomena that exist in DOC. M. Schejbal et al. [29,30] developed a transient spatially 2D model to depict the combustion of soot by oxygen and nitrogen dioxide. Cozzolini [31] developed a DOC–DPF model to predict DPF loading and regeneration during engine transient cycles. To the best of our knowledge, very few of these models are used to analyze the effects of exhaust characteristics and control strategy parameters.

There are a few researches on regeneration strategy and control design of regeneration. Michelle Morcos [32] characterized ash deposition in DPF for the purpose of regeneration control. Carlo Beatrice et al. [33] explored the detailed characterization of particulate emissions of a catalyzed DPF using actual regeneration strategies. Ted N. Tadrous, Kevin Brown [34] and Qu Dawei et al. [35] developed both active and passive regeneration strategies of DPF for real-life optimization and retrofit. Bai Shuzhan et al. [36] investigated the influence of active control strategies on exhaust thermal management and Navtej Singh et al. [37] compared different DPF regeneration strategies using integrated system simulation. Jian Gong and Christopher J. Rutland [38] implemented pulsed injection of fuel in an exhaust pipe to optimize regeneration of DPF. Shuzhan Bai et al. [39] built a soot-loading estimation model to determine precisely the triggering of DPF regeneration. Jinhiao Ning and Fengjun Yan [40] developed a composite controller utilizing simulated and experimental data to modulate DOC-out temperature for DPF regeneration. Yong-Wha Kim and Michiel Van Nieuwstadt [41] and Olivier Lepreux [42] investigated model-based temperature control of DOC-out temperature to reject exhaust flow rate and temperature disturbances. Olivier Lepreux et al. [43] investigated the motion planning problem of DPF outlet temperature. In his paper, the trajectory of hydrocarbon injection was planned to
follow a pre-defined profile of DOC outlet temperature. However, their work did not combine real exhaust conditions and remained at the theory stage.

In summary, the vast majority of research focuses on modeling of DPF regeneration and investigating its influencing factors mainly in regard to geometrical characteristics. Some preparatory investigations have been carried out in terms of DOC-out temperature control for DPF regeneration. However, exhaust characteristics and control parameters which have significant implications for DPF regeneration are rarely investigated by researchers. In this paper, the effects of main exhaust characteristics such as exhaust flow rate, oxygen concentration and emission of reactants, or control strategies such as DOC-out temperature and soot loading, have been investigated and their correlations with maximum temperature, maximum rate of temperature increase and regeneration duration of DPF have been evaluated utilizing the improved fuzzy grey relational analysis method. Based on the results of this work, a more reasonable control strategy and DOC-out temperature controller can be implemented which considers realistic exhaust conditions and DPF status.

2. Mathematical Model and Chemical Mechanisms

In this section, a mathematical model of diesel oxidation catalyst and diesel particulate filter comprising a series of partial differential equations will be proposed, along with mechanisms of chemical reactions during regeneration in both devices. The inlet boundary condition of DOC is measured on an engine test bench, including flow rate, exhaust temperature, oxygen concentration and composition of exhaust. The outlet boundary conditions of DOC, which are computed from the theoretical model, are treated as the inlet boundary condition of DPF. In this way, the whole process of computation is completed.

2.1. Diesel Oxidation Catalyst Model

For flow through reactors such as DOC, quasi-steady approximation is assumed due to the short residence time of gas in the reactor compared to other time scales of interest. This assumption simplified the substantial derivative and replaced them with a simpler spatial derivative. The flow is laminar, based on Reynolds number analysis. Density of gas is calculated by ideal gas law. Body forces such as gravity are neglected.

Continuity equation:
\[
\frac{\partial}{\partial z} (\rho \v) = 0
\] (1)

Momentum equation:
\[
\frac{\v}{\v} \frac{\partial p}{\partial z} + \v \frac{\partial \v}{\partial z} = - S f \v^2
\] (2)

where \( \v \) is the void fraction of DOC substrate, \( S \) is surface area per DOC volume and \( f \) is the friction factor.

Solid-phase energy equation:
\[
\Psi_s \frac{\partial T_s}{\partial t} = \frac{\partial}{\partial z} (f_{sb} \lambda_{sb} \frac{\partial T_s}{\partial z}) + hS(T_g - T_s) - \sum_{j=1}^{n_r} \Delta H_j r_j + \frac{P}{V} + h_x S_x (T_x - T_s)
\] (3)

where \( \Psi_s \) is the effective heat capacity of DOC, \( f_{sb} \) is the solid fraction of DOC substrate and \( \lambda_{sb} \) is the thermal conductivity of substrate. On the right-hand side of the equation, the five terms are, respectively, conduction, convection, reaction enthalpy, external input and heat exchange with ambient. The heat transfer coefficient \( h \) is related to a single Nusselt number for fully developed laminar flow as follows:
\[
h = N_u \frac{\lambda_g}{D_h}
\] (4)
Gas-phase energy equation:

\[ \varepsilon \rho g c_p g \frac{dT_s}{dz} = h S (T_s - T_g) \] (5)

Due to the relatively short dwell time of exhaust gas in DOC, all chemical reactions are considered as global reactions instead of surface reactions. In addition, the effects of adsorption and desorption are taken into account. The injected diesel fuel is treated as propylene for simplicity. The main chemical reactions inside DOC are described as follows:

\[ \text{CO} + \frac{1}{2}\text{O}_2 \xrightarrow{k_1} \text{CO}_2 \] (6)

\[ \text{HC} + \frac{5}{4}\text{O}_2 \xrightarrow{k_2} \text{CO}_2 + \frac{1}{2}\text{H}_2\text{O} \] (7)

\[ \text{NO} + \frac{1}{2}\text{O}_2 \xrightarrow{k_3} \text{NO}_2 \] (8)

\[ \text{C}_3\text{H}_6 + 9/2\text{O}_2 \xrightarrow{k_4} 3\text{CO}_2 + 3\text{H}_2\text{O} \] (9)

\[ \text{C}_3\text{H}_6 + Z \xrightarrow{k_5} Z(\text{C}_3\text{H}_6) \] (10)

where \( k_i \) is the reaction constant and \( Z \) is the catalytic site of DOC. All the reaction rates are computed based on an Arrhenius-type function.

2.2. Diesel Particulate Filter Model

A single pair consisting of an inlet channel and outlet channel is shown in Figure 2. As depicted in Figure 2, exhaust with soot flows through the porous media of the filter wall and leave soot particles deposited as a soot cake on the surface of the channel. Figure 2 also shows the computation domain of the governing equations. Pre-mentioned model assumptions are also valid here.

The mass conservation equation of channel gas, momentum equation of channel gas and energy balance equation in the wall, which are derived from the model proposed by Bissett [44], are depicted as follows:

Conservation of mass equation of channel gas:

\[ \frac{\partial (\rho_i v_i)}{\partial z} = ( -1 )^i ( 4/d ) \rho_w v_w \] (11)

where \( i = 1 \) represents the inlet channel and \( i = 2 \) represents the outlet channel.

Conservation of momentum of channel gas:

\[ \frac{\partial P_i}{\partial z} + \frac{\partial (\rho_i v_i^2)}{\partial z} = -a \mu T_i v_i / d^2 \] (12)

where \( a \) is the square channel pressure drop correlation and \( \mu \) is exhaust viscosity.
Conservation of enthalpy:

\[
\frac{\partial}{\partial t} \left( \rho p C_{pp} (T_w) T_w + \rho_s w_s C_{ps} (T_w) T_w \right) = -h_1(T_w - T_1) - h_2(T_w - T_2) + \phi(z,t) + \lambda_p \frac{\partial}{\partial z} \left( w \frac{\partial T_w}{\partial z} \right) + \lambda_s w_s \frac{\partial^2 T_w}{\partial z^2}
\]

where \( h_1 \) and \( h_2 \) are the sensible enthalpy transfer coefficients.

Normally, 90% of nitric oxides in engine exhaust are nitrogen monoxide. When the exhaust passes through the DOC, the nitrogen monoxide is oxidized into nitrogen dioxide. Therefore, the regeneration mechanism inside DPF consists of soot oxidation by both oxygen and nitrogen dioxide. The latter is called continuous regeneration. The detailed chemical reactions are depicted as follows:

\[\text{C} + \frac{1}{2}\text{O}_2 \xrightarrow{k_6} \text{CO}\]  \hspace{1cm} (14)

\[\text{C} + \text{O}_2 \xrightarrow{k_7} \text{CO}_2\]  \hspace{1cm} (15)

\[\text{C} + \text{NO}_2 \xrightarrow{k_8} \text{CO} + \text{NO}\]  \hspace{1cm} (16)

\[\text{C} + 2\text{NO}_2 \xrightarrow{k_9} \text{CO}_2 + 2\text{NO}\]  \hspace{1cm} (17)

\[\text{C} + \text{NO}_2 + 1/2\text{O}_2 \xrightarrow{k_{10}} \text{CO}_2 + \text{NO}\]  \hspace{1cm} (18)

\[\text{C} + \text{NO}_2 + 1/2\text{O}_2 \xrightarrow{k_{11}} \text{CO} + \text{NO}_2\]  \hspace{1cm} (19)

where \( k_i \) is the reaction constant and all the reaction rates are also computed based on an Arrhenius-type function. All parameters of the Arrhenius formula including reactions both in DOC and DPF are cited from the AVL Boost theory manual [45]. Time step of solver is set as 0.1 s. Spatial discretization is implemented by second-order upwind method. Time variable is discretized implicitly.

3. Experimental Exhaust Characteristics and Emission Measurements

The exhaust parameters including mass flow rate, temperature and composition of a specific diesel engine are measured on a test bench under different engine speeds and output powers. All the acquired data are treated as the inlet boundary condition of DOC. Then, the outlet boundary condition of DOC is computed using the above-mentioned theoretical model. Subsequently, the computed results are used as an inlet boundary condition of DPF to compute the key indexes concerned during regeneration.

For accuracy of exhaust characteristics measurements, the DOC and DPF devices are installed in the exhaust pipe during testing, since after-treatment devices alter the emission levels of the engine. The test bench includes a diesel engine, DOC–DPF, a positive displacement air flow meter (Romet G65) to measure intake air flow rate, a Horiba gas analyzer (MEXA-9100HEGR) to measure gaseous emissions, a differential mobility spectrometer (combustion DMS500) to measure particulate emission, a fuel consumption meter (MCS-960 gravimetric) to measure fuel consumption rate and a dynamometer (MS1713-4 electrical) to adjust the output power and speed of diesel engine. In Figure 3, the primary equipment is depicted. In the right part, a data acquisition and display module is shown.

The substrate of DOC is made of cordierite. All the thermal properties in computation are based on standard cordierite material. The wash-coat material is alumina and the detailed parameters of DOC are shown in Table 1.
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Table 1. Parameters of DOC.

| Parameters               | Value       |
|--------------------------|-------------|
| Frontal area (mm²)       | 20,000      |
| Length (mm)              | 160         |
| Cell density (1/in²)     | 400         |
| Wall thickness (m)       | 1.5 × 10⁻⁴  |
| Wash-coat thickness (m)  | 3 × 10⁻⁵    |
| Channel shape            | Square      |
| Substrate material       | Cordierite  |
| Wash-coat material       | Alumina     |

The substrate of DPF is made of cordierite. Additionally, the thermal properties used in computation are based on standard cordierite material. No cerium catalyst or fuel additive is considered here. The main parameters of DPF are depicted in Table 2.

Table 2. Parameters of DPF.

| Parameters               | Value       |
|--------------------------|-------------|
| Frontal diameter (mm)    | 160         |
| Length (mm)              | 240         |
| Cell density (1/in²)     | 100         |
| Wall thickness (mm)      | 0.4318      |
| Channel shape            | Square      |
| Substrate material       | Cordierite  |

The DOC–DPF is equipped on a YC4G180-30 diesel engine which meets the national emission regulation III. The detailed parameters of the diesel engine are indicated in Table 3.
Table 3. Parameters of diesel engine.

| Parameters          | Value                        |
|---------------------|------------------------------|
| Type                | 4-stroke                     |
| Cylinder no.        | 4                            |
| Stroke (mm)         | 110                          |
| Connecting rod (mm) | 152                          |
| Compression ratio   | 18                           |
| Displacement (l)    | 5.2                          |
| Air aspiration      | turbo-charged/inter-cooled   |

In order to investigate the effect of exhaust parameters on DOC–DPF regeneration, steady-state parameters of engine exhaust are in need. In this paper, the universal performance characteristics map of the YC4G180-30 engine is measured. The speed varies from 1000 to 3600 r/min with an increment of 200 r/min and the output power varies from 10 to 100 kW with an increment of 10 kW. The acquired data utilized in this paper include intake flow rate, fuel consumption rate, temperature after turbocharger, oxygen concentration and emission of reactants such as carbon monoxide, hydrocarbon, nitrogen oxide and unburned fuel. The mass flow rate of exhaust is computed by adding intake mass flow rate and fuel consumption rate. All the measured data are treated as the inlet boundary condition of DOC to investigate the regeneration performance of DPF under different exhaust conditions and control strategies.

4. Results and Discussion

4.1. Effects of Exhaust Flow Rate and Temperature to DOC-DPF Regeneration System

Normally, the outlet temperature of DOC is kept constant or following a pre-defined trajectory. Therefore, exhaust flow rate and exhaust temperature synchronously determine the amount of propylene the injector has to inject. In addition, the mass flow rate of the exhaust can impact the regeneration process by altering heat transfer intensity between DPF substrate and exhaust, which will be discussed later.

Figure 4 shows the experimental data of exhaust temperature after turbocharger (left) and exhaust mass flow rate (right) under different engine speed and output power. The temperature of exhaust is measured after turbocharger, before DOC. The mass flow rate of exhaust is computed by adding the mass of intake air and consumed diesel fuel.

![Figure 4. Exhaust temperature after turbocharger (left) and exhaust mass flow rate (right) under different speeds and output powers.](image)

To treat the DOC as a zero-dimensional model, the amount of propylene needed to be injected in front of the DOC in order to reach the specific DOC-out temperature can be
calculated by the energy conservation equation of a DOC under steady state. The formula of the energy conservation equation is as follows:

\[ \eta \dot{m} \Delta H = \nu \rho_g A_0 C \dot{m}_g (T_{\text{set}} - T_{\text{exg}}) \]  

(20)

where \( \eta \) is the conversion rate of injected propylene, \( \dot{m} \) is the mass flow rate of injected propylene, \( \Delta H \) is low heating value of propylene, \( A_0 \) is the open frontal area of DOC and \( T_{\text{set}} \) is the predefined DOC-out temperature which is normally the control target.

For the purpose of simplicity, the diesel fuel is treated as propylene and totally vaporized before DOC inlet. Another assumption is that the DOC is designed to enable chemical reactions and heat transfer with very high efficiency. Consequently, the conversion rate of propylene in DOC is regarded as 95% with high conversion rate and 90% with low conversion, according to engine working condition. Heat loss of the DOC to ambient was neglected. The calculated mass flow of injected fuel was used as the input of the numerical model. The simulated DOC outlet temperature was very close to \( T_{\text{set}} \). In Figure 5, the computed propylene mass flow based on Equation (20) is depicted.

![Figure 5. Injected fuel mass under different engine working conditions.](image)

The range of exhaust temperatures of the tested engine is between 180 and 520 °C and the exhaust flow rate ranges between 70 and 520 kg/h. Figure 5 indicates the general trend that the required amount of propylene increases with the increase in exhaust mass flow and decrease in temperature, and vice versa. Fuel was injected by an injector upstream of the DOC inlet to guarantee full vaporization and mixing. Injection was triggered when pressure drop along the DPF reached a specific value. With larger \( T_{\text{set}} \), namely the targeted DOC-out temperature, the map of injected propylene mass rate shifts upwards, as the red arrow in Figure 5 shows. In practical application, the exhaust temperature and mass flow rate can be obtained by the interpolated map in Figure 4. Then, these obtained values can be utilized to obtain the amount of propylene by inquiring the interpolated map in Figure 5.

Normally, if the exhaust temperature is below the light-off temperature of DOC, the injected fuel will not react and further causes large hydrocarbon slip. Therefore, the fuel injection can only be triggered when the exhaust temperature is above this light-off temperature. In this paper, the minimum exhaust temperature of the tested engine is 187 °C, which is higher than the light-off temperature. Consequently, the light-off phenomenon of DOC will not be discussed in this paper, but must be considered in real control strategies.

To further investigate the effects of exhaust flow rate on the process of DPF regeneration, three cases are selected, which are 3600, 2000 and 1200 r/min, and the output power is 60, 50 and 30 kW, respectively. These output powers are selected to keep the exhaust...
temperature consistent in each case, which is 380 °C. By doing this, the exhaust flows into the DOC with the same state in three cases. The mass flow rate of the exhaust in each case is 428.8, 286.91 and 155.1 kg/h, respectively. The soot loading in the three cases is 6 g/L and the DOC-out temperature is kept at 600 °C.

Figure 6 depicts the numerical results of the temperature evolution of the DPF substrate at different exhaust flow rates at a normalized axial position of 0.9. It is worth noting that the temperature profile of the substrate can be regarded as a heat wave propagating from the front part of DPF to the rear part. The peak temperature of the wave rises along the axial direction. In addition, there is a higher amount of soot deposited in the rear part of the DPF channel, which causes a higher rising rate of temperature according to the research of K. Yamamoto et al. [46]. Consequently, the 0.9 normalized position is chosen to represent the maximum temperature and maximum rate of temperature increase inside DPF. In Figure 6, the dashed lines indicate the timing when the rate of temperature increase reaches the maximum. Under all engine speeds, the temperature of DPF rises rapidly to its peak value and then cools down to the temperature of the DPF inlet gas. It can be observed that both maximum temperature and rate of temperature increase decrease with the increase in engine speed. This can be explained by the fact that when the mass flow rate increases, the velocity in the channel increases correspondingly. Therefore, the convection and heat transfer between exhaust gas and substrate enhances and further removes more enthalpy generated by soot oxidation, while in low engine speed, the volumetric speed of the exhaust gas is lower, relatively, which makes the heat easy to accumulate in the DPF substrate. Therefore, both the maximum temperature and rate of temperature increase decrease with the increase in engine speed. Table 4 shows specific values of maximum temperature, rate of temperature increase and regeneration duration in each case.

![Image](image.png)

**Figure 6.** Substrate temperature of DPF at 0.9 normalized axial position under different exhaust mass flow rates.

**Table 4.** Regeneration characteristics under different engine speeds.

| Engine Speed (r/min) | $T_{\text{max}}$ (°C) | $\dot{T}_{\text{max}}$ (°C/s) | $t_{\text{reg}}$ (s) | $\dot{m}$ (kg/h) |
|----------------------|----------------------|------------------------|------------------|-----------------|
| 1200                 | 814.8                | 89.8                   | 50               | 0.81            |
| 2000                 | 790.4                | 84.1                   | 38               | 1.61            |
| 3600                 | 769.6                | 82.9                   | 32               | 2.23            |
The data in Table 4 further explain the profiles of Figure 6. The third column in Table 4 shows that the duration of regeneration decreases with engine speed. This is due to the large oxygen mass that promotes the oxidation speed of soot under a higher engine speed. However, the oxygen concentrations in all cases are abundant enough to oxidize soot normally. The fourth column shows injection rate of propylene in order to reach 600 °C DOC outlet temperature.

4.2. Effects of DPF Soot Loading and DOC-Out Temperature on DPF Regeneration

In real application, mass of soot loading in DPF and DOC-out temperature are two of the most significant parameters in designing reasonable control strategies. In this chapter, the parameters in Table 4, such as maximum temperature, maximum rate of temperature increase and regeneration duration are investigated under different soot loading and DOC-out temperature. The results can instruct the design of rational control strategies.

The cruising speed of the engine, which is 2000 r/min, is chosen in computation. The other speeds have similar patterns. The tested mole fraction of oxygen is 10%. The mass of soot loading varies between 3, 6 and 9 g/L, respectively. The DOC-out temperature varies between 550, 600 and 650 °C, respectively. These values are frequently met in running vehicles. Figure 7 shows the temperature evolution under different soot mass loadings and DOC-out temperatures.

![Figure 7. Substrate temperature of DPF at 0.9 normalized axial position under different soot loadings and DOC-out temperatures.](image)

From Figure 7, the temperature rises rapidly to peak temperature and cools down to the temperature of DOC-out temperature, except for 3 g/L of soot loading. The maximum temperature increases with the increase in soot loading and DOC-out temperature. However, the influence of soot loading is more obvious. Figure 7 indicates that when the soot loading is constant and DOC-outlet temperature varies from 550 to 650 °C, the curves of temperature evolution are very similar to each other. When the DOC-outlet temperature is constant and soot loading varies from 3 to 9 g/L, the differences are very obvious. In addition, when soot loading is relatively low (3 g/L), as the solid lines in Figure 7 show, temperature rise compared to DOC-out temperature due to soot oxidation is very inconspicuous. In the case where soot loading is 3 g/L and DOC-out temperature is 650 °C, the maximum temperature of the DPF substrate is almost equal to the exhaust temperature of the DOC outlet. From the above analysis, we can conclude that soot loading is the more significant factor influencing the maximum temperature of DPF regeneration, and the specific data regarding key indexes of regeneration are depicted in Figure 8.
Figure 8 indicates that the maximum temperature of DPF substrate increases with both DOC-out temperature and soot loading, and the latter takes a much more obvious effect. The maximum rate of temperature increase has a similar trend, except for the low DOC-out temperature scenario. In this scenario, the maximum rate of temperature increase decreases when the soot loading increases from 6 to 9 g/L. This can be explained by the fact that when soot loading is as high as 9 g/L, DOC-out temperature becomes a limiting factor in the soot oxidation. This gives engineers a hint that when soot loading is high, DOC-out temperature can be decreased to restrict the maximum rate of temperature increase in DPF.

Figure 9 shows the duration of regeneration in each case. The red dashed line shows the injection rate of propylene in each case. The duration increases with soot loading in medium DOC-out temperature, namely 600 °C. The duration decreases dramatically and then increases slightly with the increase in soot loading when the DOC-out temperature is 550 °C. This can be explained by the fact that when the temperature and soot loading are both low, the soot oxidation is slow due to the very sparse distribution of soot in the DPF substrate and the low temperature. The duration increases and then decreases slightly with the increase in soot loading when the DOC-out temperature is 650 °C. This indicates that when the DOC-out temperature is as high as 650 °C, concentration of soot in DPF is the limiting factor of oxidation speed. However, the duration of regeneration does not vary much except for the first case. This gives the impression that when the soot loading is low, it is not cost-effective to start regeneration if the DOC-out temperature is low.
4.3. Effects of Oxygen Concentration and Reactants Emission in Exhaust

Normally, the mole concentration of oxygen in diesel exhaust gas varies from 5% to 15% according to different working conditions. In the previous analysis, the oxygen concentration is 10% and regeneration can conduct smoothly under this oxygen concentration. In this section, 15%, 10%, 5% and 3% oxygen concentration are selected to investigate the regeneration of DPF. The 2000 speed and 50 kW operating point of engine are chosen. The soot loading is 6 g/L and DOC-out temperature is kept at 600 °C.

Figure 10 depicts the temperature evolution of DPF substrate at an axial position of 0.9. The four curves in Figure 10 almost overlap, which indicate that the mass flow rate of oxygen is abundant enough under all oxygen concentrations, while the data in Table 4 show that when engine speed is as low as idle speed, the regeneration will last long, which reveals that mass flow of oxygen might not be adequate enough in this situation. Therefore, air auxiliary devices should be applied when engine speed is very low. It is also worth noting from the partially enlarged picture in Figure 10 that the soot oxidation is faster with the increase in oxygen concentration, which is reasonable because of the increase in reactant concentration. However, the maximum temperature is lower with the increase in oxygen concentration. This phenomenon can be explained by this: when the oxygen concentration is decreasing, the other compositions in exhaust gas, whose molar masses are larger than oxygen, such as nitrogen, carbon monoxide and hydrocarbon, are increasing. Therefore, the density of exhaust gas is increasing, which makes the volume flow rate of exhaust decrease under constant mass flow rate. Further, the convection between exhaust and substrate weakens. Ultimately, the maximum temperature of the substrate is higher with the decrease in oxygen concentration. In general, the oxygen is abundant enough under the majority of the operating points of the engine to support soot oxidation.
Besides oxygen concentration in exhaust, emission of reactants is another important influencing factor. On one hand, the unburned diesel fuel and carbon monoxide will react in DOC and further increase DOC-out temperature. On the other hand, the nitrogen oxide in exhaust gas will be converted into nitrogen dioxide, which is a strong oxidizing agent of soot in DPF. Thus, regeneration will be influenced by emission of reactants in exhaust. Next, an operating point of 2000 r/min and 50 kW output power is selected to investigate the effects of reactants emission on the DOC–DPF system. Table 5 below shows the detailed emission of reactants under this operating point.

Table 5. Emissions under 2000 r/min and 50 kW output power.

| Emissions                  | Mole Fraction |
|----------------------------|---------------|
| Nitrogen                   | 0.77          |
| Oxygen                     | 0.13          |
| Carbon dioxide             | 0.05          |
| Carbon monoxide            | $5 \times 10^{-4}$ |
| Hydrogen                   | $1.67 \times 10^{-4}$ |
| Water vapor                | 0.05          |
| Nitrogen monoxide          | $3 \times 10^{-4}$ |
| Nitrogen dioxide           | $3.3 \times 10^{-5}$ |
| Unburned diesel vapor      | $2 \times 10^{-4}$ |

The emission data in Table 5 cover all emissions from the tested engine under 2000 r/min, 50 kW output power. The proportion of NO$_2$ and NO is assumed to be 1:9. The unburned diesel vapor in exhaust is assumed to be composed of propylene and hydrocarbon. The mass flow rate of exhaust is 286.91 kg/h and the exhaust temperature is 380 °C. The soot loading and DOC-out temperature is kept at 6 g/L and 600 °C, respectively. The injection rate of propylene is 1.61 kg/h according to previous results and the initial temperature of DOC is 26.85 °C.

Figure 11 depicts the mass percentages of unburned reactants at the outlet of the DOC along with time. There is no chemical reaction in the first five seconds due to low temperature but adsorption exists in DOC channel. The black solid line indicates the unburned mass fraction of injected propylene and diesel vapor in exhaust. At the very beginning, 33% injection and diesel vapor are left at the DOC outlet due to the fact that the
DOC is heated from room temperature. With the increase in temperature, the conversion rate of injected fuels increases rapidly, to higher than 95% in 20 s. It can be concluded that in real application, when the temperature of DOC substrate is always high, the conversion rate of injected fuel is very high and the reaction happens almost instantaneously in some front part of the DOC channel. The same characteristic applies to carbon monoxide and hydrogen. The mass fraction of carbon monoxide at the DOC outlet decreases from 7% to 0% very quickly and there is almost no hydrocarbon left during the whole process, which reveals that hydrocarbon is more active than carbon monoxide in DOC. The above phenomenon verifies that DOC is a device which enables extremely sufficient heat transfer and chemical reactions. The profile of nitrogen monoxide is different. It increases firstly due to the desorption effect of the DOC substrate and then decreases dramatically as the temperature rises. The dashed line in Figure 11 indicates that 5.88% of nitrogen monoxide is left in the end. It can be concluded that the oxidation of nitrogen monoxide happens along the whole length of the DOC channel. An interesting phenomenon observed from Figure 11 is that nitrogen monoxide is the least active reactant inside DOC. Nitrogen dioxide is a very important oxidizer of carbon in DPF, which is not shown here. However, it demonstrates an opposite trend with nitrogen monoxide, because the whole amount of nitrogen monoxide at the DOC inlet is constant.

![Mass fraction of the main reactants at DOC outlet.](image)

**Figure 11.** Mass fraction of the main reactants at DOC outlet.

In Figure 12, the outlet temperature of DOC is depicted along with time, with control target equal to 600 °C. The solid line represents the temperature profile with all emissions and the dash-dotted line represents the temperature profile without emissions. The injection rate of propylene is 1.61 kg/h. As can be observed in Figure 12, the outlet temperature of the DOC rises faster and has a higher steady state temperature with emissions considered. This is due to the exothermic reactions of carbon monoxide, hydrogen, nitrogen monoxide and unburned diesel fuel in exhaust. The specific temperature rise is 41.1 °C, as the dashed lines indicate. It can be speculated that when the emissions are heavier, this temperature rise will be higher and vice versa. The dashed line in the lower part of Figure 12 shows that the outlet temperature of the DOC is lower than the exhaust temperature, which is 380 °C in the earlier stage. This is because the DOC is a system with large heat capacity and the initial temperature of the DOC is at room temperature. Consequently, a portion of enthalpy is used to heat up the substrate of the DOC, which causes the temperature to become lower than the exhaust temperature during the preliminary stage.
The portion of enthalpy is used to heat up the substrate of the DOC, which causes the temperature to become lower than the exhaust temperature during the preliminary stage.

Figure 12. Outlet temperature of DOC with and without emission.

Through previous analysis, we know that propylene, diesel fuel vapor, carbon monoxide and hydrogen are burned rapidly with a very high conversion rate. Nitrogen monoxide is oxidized into nitrogen dioxide with a conversion rate of 94.12%. In addition to the effect of rising DOC-out temperature, the generated nitrogen dioxide will have an effect on soot oxidation in the DPF, for nitrogen dioxide is a strong oxidizing agent of soot. In Figure 13, the influence of nitrogen dioxide on DPF regeneration is depicted.

Figure 13. Substrate temperature of DPF at 0.9 normalized axial position considering the soot oxidation by nitrogen dioxide.

The concentration of nitrogen dioxide at the inlet of the DPF is composed of two parts. One is the pre-existing nitrogen dioxide in exhaust and the other is converted from nitrogen monoxide. The specific concentration of nitrogen dioxide at the DPF inlet is computed as $3.2 \times 10^{-4}$. It can be observed from Figure 13 that the dashed line and red line almost overlap, which indicates that the influence of nitrogen dioxide can be neglected. This is
due to the fact that the oxidation of soot by nitrogen dioxide is greatly inhibited under a high temperature, which is 600 °C in this case. Another reason is that since there is no catalytic coating or fuel additive in DPF substrate, the continuous regeneration supported by nitrogen dioxide is difficult to proceed. The blue line shows the temperature profile during DPF regeneration, considering the exothermic effect of emissions with nitrogen dioxide. It indicates that the temperature profile is altered merely due to the increase in DPF inlet temperature.

Through the above analysis, it reveals that emissions in exhaust can react in the DOC and raise the outlet temperature of the DOC. The reaction speed is almost instantaneous with a very high conversion rate, except for nitrogen monoxide. The oxidation of soot by nitrogen dioxide is greatly inhibited under the temperature range of active regeneration without catalytic support, which makes the effect of nitrogen dioxide during active regeneration negligible [47]. In general, the gross effect of emissions is equivalent to raising the outlet temperature of the DOC to tens of Celsius.

4.4. Fuzzy Grey Relational Analysis on the Effects of Significant Factors on DPF Regeneration

According to previous analysis, the mass flow rate of exhaust, oxygen concentration, soot loading, DOC-out temperature and reactants of emission will influence key indexes concerned during regeneration. However, the effect of reactants in exhaust is equivalent to DOC-out temperature. Therefore, the first four factors are considered and grey relational analysis (GRA) is utilized to quantify the effects of each factor on key indexes in the process of DPF regeneration. By this means, the inherent relationships between influencing factors and regeneration can be revealed, which enables simplification of control strategy designing. The detailed procedures of GRA are as follows:

(1) Establish comparison matrix $X'$ and reference matrix $Y$:

$$X' = \begin{bmatrix} x'_1 \\ x'_2 \\ \vdots \\ x'_m \end{bmatrix} = \begin{bmatrix} x'_1(1) & x'_1(2) & \cdots & x'_1(n) \\ x'_2(1) & x'_2(2) & \cdots & x'_2(n) \\ \vdots & \vdots & \ddots & \vdots \\ x'_m(1) & x'_m(2) & \cdots & x'_m(n) \end{bmatrix}$$  \hspace{1cm} (21)

where $m$ represents the subscript of the influencing factor and equals four in this paper. $n$ represents the number of trials with different factor vectors. The reference matrix $Y$ is as follows:

$$Y = \begin{bmatrix} y_1(1) & y_1(2) & \cdots & y_1(n) \\ y_2(1) & y_2(2) & \cdots & y_2(n) \\ \vdots & \vdots & \ddots & \vdots \\ y_p(1) & y_p(2) & \cdots & y_p(n) \end{bmatrix}$$  \hspace{1cm} (22)

where $p$ represents the subscript of key indexes. In this paper, maximum temperature, maximum rate of temperature increase and regeneration duration are key indexes. Consequently, $p$ is equal to three.

(2) Normalization of comparison matrix by:

$$x_i(k) = \frac{x'_i(k) - \min x'_i}{\max x'_i - \min x'_i}$$  \hspace{1cm} (23)

where $i$ varies from 1 to $m$ and the normalized form of the comparison matrix is:

$$X = \begin{bmatrix} x_1 \\ x_2 \\ \vdots \\ x_m \end{bmatrix} = \begin{bmatrix} x_1(1) & x_1(2) & \cdots & x_1(n) \\ x_2(1) & x_2(2) & \cdots & x_2(n) \\ \vdots & \vdots & \ddots & \vdots \\ x_m(1) & x_m(2) & \cdots & x_m(n) \end{bmatrix}$$  \hspace{1cm} (24)
(3) Compute cosine value of fuzzy factors which reflects the similarity of two factors:

\[
r_{1,ij} = \frac{\sum_{k=1}^{n} y_j(k)x_i(k)}{\sqrt{\sum_{k=1}^{n} y_j(k)^2} \sqrt{\sum_{k=1}^{n} x_i(k)^2}}
\]  

(25)

where \( i \) ranges from 1 to \( m \) and \( j \) ranges from 1 to \( p \).

(4) Calculate correlation coefficient:

\[
\zeta_{ij}(k) = \frac{\Delta_{\text{min}ij} + l\Delta_{\text{max}ij}}{\Delta(k) + l\Delta_{\text{max}ij}}
\]

(26)

where \( l \) is the resolution ratio, which is normally 0.5. \( \Delta_{\text{min}ij}, \Delta_{\text{max}ij} \) and \( \Delta(k) \) can be computed as follows:

\[
\Delta_{\text{min}ij} = \min |y_j(k) - x_i(k)|
\]

(27)

\[
\Delta_{\text{max}ij} = \max |y_j(k) - x_i(k)|
\]

(28)

\[
\Delta(k) = |y_j(k) - x_i(k)|
\]

(29)

(5) Define the weighing coefficient vector, which applies fuzzy Euclidean mathematics for the accuracy of computation, and compute the Euclidean coefficient:

\[
w = (w_1, w_2, \ldots w_m)
\]

(30)

\[
r_{2,ij} = 1 - 2\sqrt{\sum_{k=1}^{n} [w_j(1 - \zeta_{ij}(k))]^2}
\]

(31)

(6) Ultimately, the fuzzy grey correlation coefficient can be calculated as follows:

\[
\rho_{ij} = \sqrt{\frac{r_{1,ij}^2 + r_{2,ij}^2}{2}}
\]

(32)

In order to cover more information and simplify the process of analysis, a method of orthogonal design is utilized to establish a comparison and reference matrix. The detailed orthogonal design of trials and computation results is depicted in Table 6.

**Table 6. Trials and computation results based on orthogonal design.**

| Trial | \( m \) (kg/h) | \( T_{\text{set}} \) (°C) | \( m_{\text{soot}} \) (g/L) | \( C_{\text{oxygen}} \) | \( T_{\max} \) (°C) | \( \dot{T}_{\max} \) (°C/s) | \( t_{\text{reg}} \) (s) |
|-------|----------------|-----------------|-----------------|-----------------|-----------------|-----------------|-----------------|
| 1     | 155.1          | 550             | 3               | 0.05            | 625.6           | 40.8            | 76              |
| 2     | 155.1          | 600             | 6               | 0.1             | 814.8           | 89.8            | 50              |
| 3     | 155.1          | 650             | 9               | 0.15            | 967.2           | 118.9           | 44              |
| 4     | 286.91         | 550             | 6               | 0.15            | 769.5           | 85.1            | 38              |
| 5     | 286.91         | 600             | 9               | 0.05            | 942.1           | 121.6           | 45              |
| 6     | 286.91         | 650             | 3               | 0.1             | 661.1           | 51.6            | 35              |
| 7     | 428.8          | 550             | 9               | 0.1             | 874.6           | 110.2           | 36              |
| 8     | 428.8          | 600             | 3               | 0.15            | 631.7           | 48.4            | 29              |
| 9     | 428.8          | 650             | 6               | 0.05            | 798.1           | 94.7            | 33              |
With the data in Table 6, the comparison matrix and reference matrix can be derived as follows:

\[
X' = \begin{bmatrix}
155.1 & 155.1 & 155.1 & 286.91 & 286.91 & 286.91 & 428.8 & 428.8 & 428.8 \\
550 & 600 & 650 & 550 & 600 & 650 & 550 & 600 & 650 \\
3 & 6 & 9 & 6 & 9 & 3 & 9 & 3 & 6 \\
0.05 & 0.1 & 0.15 & 0.15 & 0.05 & 0.1 & 0.1 & 0.15 & 0.05 \\
\end{bmatrix}
\]

\[
Y = \begin{bmatrix}
625.6 & 814.8 & 967.2 & 769.5 & 942.1 & 661.1 & 874.6 & 631.7 & 798.1 \\
40.8 & 89.8 & 118.9 & 85.1 & 121.6 & 51.6 & 110.2 & 48.4 & 94.7 \\
76 & 50 & 44 & 38 & 45 & 35 & 36 & 29 & 33 \\
\end{bmatrix}
\]

Figure 14 depicts the fuzzy grey correlation coefficient of exhaust flow rate, DOC-out temperature, soot loading and oxygen concentration on key indexes during DPF regeneration. The horizontal axis represents the maximum temperature \((y_1)\), maximum rate of temperature increase \((y_2)\) and regeneration duration \((y_3)\), respectively. Based on specific values of fuzzy grey correlation coefficients in Figure 14, soot loading is the most related factor to maximum temperature during regeneration. DOC-out temperature takes the second place. Exhaust flow rate and oxygen concentration have approximately the same effects on maximum temperature. Regarding the maximum rate of temperature increase, soot loading is in a dominant position and the other three factors take roughly equal effects. Soot loading again is the most related factor to regeneration duration, whose fuzzy grey rational coefficient is 0.59. DOC-out temperature is the second most related factor to regeneration duration. Exhaust flow rate has the minimum effect on regeneration duration. In general, soot loading is the most significant factor influencing DPF regeneration. Therefore, it is crucial to evaluate soot deposited in real application. DOC-out temperature has a relatively smaller effect than soot loading but should be controlled accurately to guarantee safe regeneration. The other two factors have less influence on regeneration. Consequently, exhaust flow rate and oxygen concentration can be put in secondary positions when simplified analysis is needed. However, it is worth noting that the emission of reactants in exhaust is significant due to its equivalent effect to DOC-out temperature.

Figure 14. Fuzzy grey relational analysis of DPF regeneration.

5. Conclusions

(1) The required amount of propylene injection to reach a specific DOC-out temperature can be obtained by the following procedures: the maps of exhaust mass flow rate and temperature are calibrated based on engine speed and output power by experiments; and the map of propylene injection is calculated based on exhaust mass flow rate
and temperature by energy conservation equation. With engine speed and output power known, the amount of propylene injection can be acquired by inquiring the aforementioned maps in sequence.

(2) With the increase in exhaust mass flow rate, the maximum temperature of DPF substrate during regeneration decreases due to enhanced convection between exhaust gas and substrate. When the engine speed is as low as the idle speed, an auxiliary air device is needed to supply enough oxygen.

(3) The maximum temperature and maximum rate of temperature increase rises monotonously with the rise in soot loading and DOC-out temperature. The influence of soot loading is more obvious. The regeneration duration has little difference except for very low soot loading with relatively low DOC-out temperature, under which regeneration will last for a while. Therefore, it is uneconomic to start regeneration in this scenario.

(4) With the increase in oxygen concentration, the oxidation rate of soot increases. However, the maximum temperature of the DPF substrate decreases with the increasing oxygen concentration. This is due to the decrease in exhaust density, which raises the volume flow rate of exhaust and further enhances convection between exhaust and substrate. In general, oxygen concentration is abundant enough to support soot oxidation under the majority of engine operating points.

(5) All the emissions of reactants react in the DOC almost instantaneously in some front part of the DOC channel with very high conversion rate, except for nitrogen monoxide. Nitrogen dioxide has little impact on soot oxidation mainly due to the fact that the reaction between soot and nitrogen dioxide is greatly inhibited in the temperature range of active regeneration. Therefore, the effect of the emission of reactants is equivalent to raising the DOC-out temperature to dozens of degrees.

(6) Soot loading is the most dominant factor which influences DPF regeneration. Its fuzzy grey correlation coefficient to maximum temperature, maximum rate of temperature increase and regeneration duration are 0.726, 0.662 and 0.59, respectively. DOC-out temperature takes the second place, whose fuzzy grey correlation coefficient in key indexes is 0.681, 0.54 and 0.558, respectively. Consequently, it is crucial to evaluate soot deposition inside the DPF accurately and control DOC-out temperature precisely. The other two factors, like exhaust mass flow rate and oxygen concentration, can be omitted for the sake of simplification. It is worth noting that emission of reactants has to be considered in designing a DOC-out temperature controller for its equivalent effect to raising DOC-out temperature by dozens of degrees.

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Nomenclature

\( a \) square channel pressure drop correlation
\( A_0 \) frontal area of DOC
\( C_p_g \) heat capacity of exhaust at constant pressure
\( C_{pp} \) heat capacity of soot cake
\( C_{ps} \) heat capacity of DPF substrate
\( c_{oxygen} \) oxygen concentration in exhaust
\( d \) diameter of DPF channel
\( D_h \) diameter of DOC channel
\( f \) friction factor between exhaust and DOC substrate
\( f_{sb} \) solid fraction of DOC substrate
\( h \) heat transfer coefficient between exhaust and DOC substrate
\( h_1 \) heat transfer coefficient of inlet exhaust and DPF substrate
\( h_2 \) heat transfer coefficient of outlet exhaust and DPF substrate
\( h_x \) heat transfer coefficient between DOC and ambient
\( k_j \) chemical reaction constants in DOC and DPF
\( m \) engine exhaust mass flow rate
\( m_{soot} \) soot loading in DPF
\( m \) injecting rate of propylene
\( Nt \) Nusselt number for fully developed laminar flow
\( p \) pressure in DOC channel
\( P \) external input power into DOC
\( r_j \) reaction rate of reactant \( j \)
\( r_{ij} \) fuzzy grey correlation coefficient
\( r_{1_{ij}} \) cosine value of fuzzy factors
\( r_{2_{ij}} \) Euclidean coefficient
\( S \) surface area per DOC volume
\( S_x \) heat exchange area between DOC and ambient
\( t \) time
\( t_{reg} \) regeneration duration
\( T_1 \) inlet gas temperature of DPF
\( T_2 \) outlet gas temperature of DPF
\( T_g \) exhaust temperature in DOC channel
\( T_s \) substrate temperature of DOC
\( T_w \) temperature of DPF wall
\( T_x \) ambient temperature
\( T_{exg} \) temperature of engine-out exhaust
\( T_{max} \) maximum temperature of DPF substrate during regeneration
\( T_{max} \) maximum rate of temperature increase
\( T_{set} \) pre-defined DOC outlet temperature
\( v \) velocity of exhaust in DOC channel
\( v_i \) velocity of exhaust in DPF inlet and outlet channel \((i = 1, i = 2)\)
\( v_{le} \) velocity of exhaust in DPF wall
\( V \) DOC volume
\( w \) thickness of DPF channel
\( w_s \) thickness of sootcake
\( x \) vertical coordinate of DPF channel
\( X' \) comparison matrix
\( X \) normalized comparison matrix
\( Y \) reference matrix
\( z \) axial coordinate of DOC and DPF channel

Greek Symbols

\( \epsilon \) void fraction of DOC substrate
\[ \phi \] chemical reaction enthalpy in DPF wall
\[ \eta \] conversion rate of injected propylene
\[ \lambda_g \] thermal conductivity of exhaust in DOC
\[ \lambda_p \] thermal conductivity of soot cake
\[ \lambda_s \] thermal conductivity of DPF substrate
\[ \lambda_{sb} \] thermal conductivity of DOC substrate
\[ u \] exhaust viscosity
\[ \rho_g \] exhaust density in DOC channel
\[ \rho_i \] exhaust density of DPF inlet and outlet channel \((i = 1, i = 2)\)
\[ \rho_p \] soot cake density
\[ \rho_s \] density of DPF substrate
\[ \rho_w \] exhaust density in DPF wall
\[ \Psi_s \] effective heat capacity of DOC
\[ \zeta_{ij} \] correlation coefficient
\[ \Delta H_j \] low heating value of reactant \(j\) in DOC
\[ \Delta H \] low heating value of injected propylene

**Abbreviations**

- CRT: continuous regeneration technology
- DOC: diesel oxidation catalyst
- DPF: diesel particulate filter
- ECU: electric control unit
- GRA: grey relational analysis
- HCCI: homogeneous charge compression ignition
- nrct: number of reactants

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