Index-based optimal DG allocation for voltage quality improvement in an unbalanced network

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Abstract

Voltage quality is one of the major concerns in distribution systems. Distributed Generations (DGs) have the potential to improve voltage quality, if optimally planned and operated. Considering the problem of DG siting and sizing, this paper aims at integrating technical factors, particularly voltage quality, in planning of DGs. Hence, a methodology is proposed which optimizes voltage quality in the presence of DGs and can be used as one of the objectives in a multi-objective problem or as an intermediate stage in usual DG planning. Modified voltage quality indices are proposed which consider factors including voltage profile, voltage variation due to DG disconnection, voltage regulation and voltage unbalance. The indices are defined in such a manner suitable for three-phase unbalanced networks. The system voltage quality is assessed by a new comprehensive voltage quality index. By applying this index, the DGs locating and penetration problem is formulated to improve system voltage quality. The method is tested on IEEE 13-bus feeder which is an inherently unbalanced network.

Keywords: Voltage quality; Distributed generation planning; Multi-objective voltage index; Voltage profile; Voltage unbalance

1. Introduction

Distribution networks are facing significant technical constraints and uncertainties due to the integration of uncertain generations such as solar and wind and modern sensitive loads. In this regard, power quality has always been a concern for system planners and operators. Distribution network operators (DNOs) need to improve the quality of service, integrate high penetration of distributed generations (DGs), forecast energy flow and improve efficiency, all while maintaining stable voltage at an acceptable level under all loading and operating conditions [1]. DGs have the potential to be added to modern distribution systems and improve system performance from voltage quality point of view. On the other hand, uncoordinated and badly planned DGs might decrease system voltage quality and technical constraints, especially those related to voltage, could limit the penetration of DGs in distribution systems. Therefore, voltage quality consideration is a necessity in today’s power systems. Furthermore, DGs as an interesting alternative have revealed their potential in technical support of electrical networks competing neck and neck with traditional resources and network expansion alternatives. Accordingly, presenting methodologies which provide the option of voltage quality evaluation and improvement is useful in DG planning and scheduling programs and has been pursued as the aim of this paper. Voltage quality improvement can find its place in DG planning programs either as an intermediate stage or as one of the objectives in multi-objective planning programs. This trend can provide the planner a chance to choose a trade-off solution from a set of economically planned solutions by a criterion that maximizes system voltage quality.

In literature, DGs planning programs considered economic, technical, environmental and combination of these three objectives. Most works on DG planning have considered economic cost objective function [2-7] or a combination of...
The modified indices proposed for voltage quality evaluation in an unbalanced network can provide a useful tool for any technical evaluation in the network.
To the author’s best of knowledge, this is the first time that voltage quality indices such as voltage unbalance are considered in DG planning.

The remainder of the paper is organized as follows. Section 2 evaluates DG impacts on voltage quality. The modified voltage quality indices are presented in section 3 and the optimization problem formulated in section 4. The power system under study and result and discussion are presented in sections 5 and 6, respectively. Finally, section 7 presents conclusions.

2. Dg impacts on voltage quality

2.1. Steady State Voltage Profile

Steady state voltage is amongst the most important power quality aspect for customers. Keeping steady state voltage levels with permissible limits is important because of [1]:

- Providing for end customer equipment long life, performance and efficiency
- Safety, particularly due to overheating/fire caused by voltage or current stresses

Generally, the presence of DGs could improve the system steady state voltage profile. However, system voltages might violate the permissible bounds due to badly planned and operated DGs and this fact could limit the penetration of DG in the system. For example, overvoltage caused by DG in low demand periods might restrict the penetration limit.

Table 1 Maximum Allowable Number of DGs Considering Steady State Voltage Profile Violation [25].

| generator type                     | maximum number of generators | limiting factor                                           |
|------------------------------------|------------------------------|----------------------------------------------------------|
| constant voltage synchronous generator | 6                            | no problem                                               |
| constant power factor synchronous generator | 2                            | superior limit violation during minimum demand            |
| induction generator                 | 5                            | inferior limit violation during maximum demand            |

Table 1 shows the result of an evaluation performed in [25], which considers the maximum number of synchronous/induction 5 MW DGs in different mode of operation which could be added to a specific bus of the system without voltage violation from permissible limits. It is seen that the voltage permissible bounds limit DG penetration level in constant power factor synchronous and induction generator. Therefore, a precise evaluation of voltage quality seems necessary prior to DG installation.

2.2. Voltage Unbalance

Voltage unbalance is one of the prevalent power quality problems in distribution networks. Voltage unbalance can be attributed to factors such as: the unsymmetrical impedance of transmission and distribution lines, unbalanced or unstable power utilities, unbalanced three phase loads, uneven spread of single phase loads across the three phases and weak rural power electric systems with long transmission lines [18]. A mild unbalance in the voltage could lead to a large current unbalance which adversely affects power system equipment such as induction motors, power electronic devices and machine drives. Under unbalanced condition, the power system will incur more losses and heating effects and would be less stable. [21].

The adverse effects of unbalanced voltages on induction motors stem from the fact that the unbalanced voltage breaks down into positive, negative and zero sequence components. However, the zero component in motors is typically zero as they are mostly connected delta or ungrounded wye. Therefore, the unbalanced motor voltage contains positive and negative sequence components which have opposing phase sequences, i.e., “abc” and “acb”, respectively. Consequently, two opposing torques are produced, one of which desired and the other one opposing to the beneficial one leading to a reduction in the net torque and speed. This can cause torque and speed pulsation and increase motor noise. In addition, the negative sequence component in the unbalanced voltages generates large negative sequence currents due to the low
negative sequence impedance, which increases the machine losses and temperatures. At normal operating speeds, unbalanced voltages cause the line currents to be unbalanced in the order of 6 to 10 times the voltage unbalance. Overall, the net effect of the voltage unbalance is reduced efficiency and decreased life of the motor [21].

Figure (1) shows the recommended derating for motors as a function of percent phase-voltage unbalance recommended by NEMA standard MG 1-1993 [26]. According to the figure, the rated horsepower of the motor should be multiplied by a derating factor based upon the degree of voltage unbalance.

In [27], an investigation of the effects of DG on voltage unbalance was done which concluded that voltage unbalance was improved by adding and increasing the size of DG. However, this result is only valid for the case study of reference [27] and could not be generalized. In [28], the effect of a cogeneration plant on the system unbalance of a three phase four-wire system has been evaluated and it was concluded the electric power generation of a cogeneration might worsen the voltage and current imbalance of distribution system, especially when large amount of power had been injected to the utility network. Consequently, the confirmed fact is that DG presence surely affects the system voltage unbalance and these effects are worth to be evaluated prior to installation in DG planning programs.

![Derating factor for motors operating with phase voltage unbalance](image)

**Figure 1** Derating factor for motors operating with phase voltage unbalance [26]

3. Voltage quality indices considering DG presence

3.1. Steady State Voltage Profile Index

Steady state voltage profile is one the major characteristic of voltage quality affected by DG presence. The system buses voltage is desirable to stand near the nominal voltage. In [19], voltage profile index (VPI) is introduced as follows.

\[
VPI = 1 - \max \left( \frac{\bar{U}_{\text{nom}} - \bar{U}_{\phi_i, n_b}}{\bar{U}_{\text{nom}}} \right)_{i=1}
\]

Where \(\phi\) is the phases \(a, b\) and \(c\); \(\bar{U}_{\text{nom}}\) is the nominal voltage of the system, \(\bar{U}_{\phi_i}\) is the phase \(\phi_i\)th voltage magnitude of the \(i\)th bus and \(n_b\) is the number of buses. VPI is defined in a manner that it is desired to get as close as possible to unity.

3.2. Voltage Variation Index Due to DG disconnection

One of the important issues of voltage quality is the variation of bus voltages due to DG disconnection. This fact is important because of the limited response of voltage controller in the system. It is desirable for the distributed network operator (DNO) that these variations are as low as possible. In [25], voltage variation index due to DG connection was introduced for a balanced system which considered only one phase in calculation. Therefore, for an unbalanced system, this index needs modification. One of the purposes of this study is to size and site DG to improve voltage unbalance and that system voltages are going to be more balanced. Hence, based on the positive sequence voltages, the modified voltage variation index (VVI) is proposed as follows.

\[
VVI = 1 - \frac{1}{n_b - 1} \sum_{i=2}^{n_b} \left| U_{\text{LDG}}^{+} - U_{i, \text{NDG}}^{+} \right|
\]
Where $U^+_i$ and $U^+_{i,\text{NDG}}$ are the positive sequence magnitudes of voltage of $i\text{th}$ bus in the presence of DG and without DG, respectively. $VVI$ is desired to be around unity which means system voltages vary so little due to DG disconnection. Slack bus is not considered in calculating $VVI$. This is because slack bus is assumed to be connected to a strong upstream network whose voltage is not affected by DG presence.

3.3. Voltage Regulation Index

Another important issue related to steady-state voltage is the regulation characteristic of the network, i.e., how much the bus voltages change between maximum and minimum demand cases. It is desirable that the bus voltages change as little as possible during load variations. In [25], voltage regulation index is defined for a balanced system which needs modification for use in an unbalanced system. Again, the modified voltage regulation index ($VRI$) is proposed based on positive sequence voltage as follows.

$$\text{VRI} = 1 - \frac{1}{n_b - 1} \sum_{i=2}^{n_b} |U^+_i \text{max} - U^+_i \text{min}|$$

(3)

Where $U^+_i \text{max}$ and $U^+_i \text{min}$ are the positive sequence magnitudes of voltage of $i\text{th}$ bus during maximum and minimum demands, respectively. $VRI$ is desired to be around unity which means system voltages vary so little between maximum and minimum demand periods.

3.4. Voltage Unbalance Index

The International Electrotechnical Commission (IEC) defines voltage unbalance factor of an unbalanced voltage phasor based on positive and negative sequence as follows.

$$VUF = \frac{U^-}{U^+}$$

(4)

Where $U^+$ and $U^-$ are the positive and negative sequence voltage magnitudes. Eq. (4) gives a good definition of voltage unbalance for the evaluation of this paper. In calculating sequence component not only the voltage magnitudes but also the angles of voltages are considered. It is worth mentioning that zero sequence component is not considered in (4). This assumption is acceptable. Because according to section 2 explanation, most of the damage due to voltage unbalance in induction motors as a main load type in the system, is caused by negative sequence component. Moreover, in some types of transformer, zero sequence is omitted from line component which reduce the importance of zero sequence component in voltage unbalance analysis.

Eq. (4) is defined for one bus of the system and proposing a system index which represents the system voltage unbalance is necessary for the evaluation of this phenomenon. Therefore, the Voltage Unbalance Index ($VUI$) is proposed as follows.

$$VUI = 1 - \max_i^{n_b} (VUF_i)$$

(5)

where $VUF_i$ is the voltage unbalance factor of $i\text{th}$ bus. $VUI$ is desired to be around unity which means the harmful negative sequence voltage component is negligible and system is in a good shape from voltage unbalance point of view.

3.5. Multi-objective Voltage Index

Each of the steady state voltage indices introduced before, considers one specific aspect of steady state voltage quality, separately and for simultaneous consideration of these factors, a system index for voltage quality seems necessary. Accordingly, this comprehensive index can be used in system planning programs and technical evaluations. The multi-objective voltage index ($MVI$) is proposed as the weighted average of the previously proposed voltage indices as follows.

$$MVI = \sigma_{VPI} \times VPI + \sigma_{VVI} \times VVI + \sigma_{VRI} \times VRI + \sigma_{VUI} \times VUI$$

$$\sigma_{VPI} + \sigma_{VVI} + \sigma_{VRI} + \sigma_{VUI} = 1 \quad \sigma \in [0,1]$$

(6)

(7)

All these indices are in the range of zero to unity and $MVI$ will be in the same range, consequently. This index is desirable to be around unity which represents a perfect steady state voltage quality of the system. The coefficients $\sigma$ should be chosen based on technical priorities and the judgment of system planners prior to DG installation.
4. Optimal location and penetration of DGs for voltage quality improvement

In this section, different aspects of steady-state voltage are considered as the objective for optimal planning of DGs. The proposed steady-state voltage indices of section 3 are used as the objective function to attain the optimal location and probable capacity of DGs in view of voltage quality improvement. The results of the problems can be used:

- For DG planning when voltage quality is the concern of distribution system owner or operator due to existing a large number of sensitive and important loads. In this case, it is possible that long term economic benefits of DGs such as system losses and deferral investment be in second priority.
- As an intermediate stage in usual DG planning for determining candidate buses and maximum DG capacity in each candidate buses in view of affecting voltage quality.

4.1. Objective Function

The purpose of the problem is to maximize MVI which considers different aspects of steady state voltage quality. The control variables are active and reactive powers and location of DGs.

Maximize $\text{MVI} = F(P_{DG_n}, Q_{DG_n}, b_{DG_n}, f_{DG_n})$  \hspace{1cm} (8)

Where $P_{DG_n}, Q_{DG_n}$ and $b_{DG_n}$ are active power, reactive power, and location of the $n$th DG, respectively. $f_{DG_n}$ is the $n$th DG output power reduction factor (loading factor) in low load period and $N_{DG}$ the total number of DGs contributed in optimization program. MVI is a function of control variables. For a more desirable operation of DG, it is assumed that during the low load period, DG output power is decreased and set on a lower value than the nominal one.

4.2. Equality Constraints

The real and reactive power balance for each system bus must be satisfied. Because of the unbalance analysis of this paper, a three-phase unbalance load flow method is employed. Due to the radial nature of the system under evaluation, the iterative ladder method is selected for the load flow analysis [29] and [30]. This method employs forward and backward sweeps within which currents and voltages are calculated in each iteration, respectively. Convergence occurs when the calculated source voltage in the backward sweep corresponds to specified source voltage [30].

The equality constraints in each bus are the equations for real and reactive power balance based on load types. The equations are presented in [30] which are not mentioned here for brevity.

4.3. Inequality Constraints

4.3.1. Steady-state Bus Voltage

The bus voltages of the system are constrained to maximum and minimum permissible limits as in (9).

$U_{down_i} \leq U_i \leq U_{up_i}, \hspace{0.5cm} i \in N$  \hspace{1cm} (9)

where $U_{down_i}$ and $U_{up_i}$ refer to the downmost and upmost voltage limits at the $i$th bus.

4.3.2. Thermal Constraint

Every cable in power system has a rated current limit which must not be violated as in (10).

$I_i < I_{rated}^i, \hspace{0.5cm} i \in N_L$  \hspace{1cm} (10)

where $I_i$ and $I_{rated}^i$ are current and rated limit of line $i$, respectively and $N_L$ is the set of lines of the system.

4.3.3. DG Penetration Limit

The penetration level of DGs is constrained to maximum permissible capacity as in (11).

$\sum_{n \in N_{DG}} P_{DG_n} \leq P_{DG}^{Max}$  \hspace{1cm} (11)
4.3.4. DG Power Factor Limit

DGs are desired to work in unity power factor to inject the maximum active power. However, as voltage quality is the objective of this paper, DG power factor has been permitted to sit in a range around unity so that reactive power capability of DGs is accounted for.

\[
PF_{DG} \geq PF_{Min}
\]  

(12)

4.3.5. Limit for DG Power Reduction Factor

To have a better operation, the DG output power is reduced with the loading factor \( f_{DG} \) in low load period. During the optimization procedure \( f_{DG} \) is limited as follow.

\[
0.3 \leq f_{DG} \leq 1
\]

(13)

4.4. Optimal DGs Planning Procedure

The PSO algorithm is applied to solve the optimization problem. PSO is a heuristic algorithm which considers different populations in each iteration. The algorithm is initialized with a random first population. For every particle in the population, objective function is calculated, and optimization constraints are checked so that in case of any violation, those violations are added to the objective function using negative penalty factors. The local optimal (pbest) and global optimal solutions (gbest) will be determined, and a new population will be produced. This procedure will be reiterated until the termination condition of the algorithm is satisfied. The corresponding details of PSO algorithm are presented in [23] and equations are as follows.

\[
v^{k+1}_i = \omega v^k_i + c_1 r_1 (pbest^k_i - x^k_i) + c_2 r_2 (gbest^k_i - x^k_i)
\]

(14)

\[
x^{k+1}_i = x^k_i + v^{k+1}_i
\]

(15)

Where

\( v^k_i \) velocity of ith particle at k iteration;
\( x^k_i \) position of ith particle at k iteration;
\( \omega \) inertia weight factor;
\( c_1, c_2 \) cognitive and social coefficients equals to 0.9;
\( r_1, r_2 \) random numbers in the range of [0,1];
\( pbest^k_i \) best position of ith particle at kth iteration;
\( gbest^k_i \) global best position of the swarm at kth iteration.

In order to have better balance between global exploration and local exploitation, the inertia weight \( \omega \) is updated in each iteration as follows.

\[
\omega = \omega_{max} - \frac{\omega_{max} - \omega_{min}}{iter_{max}} \times k
\]

(16)

Where

\( \omega_{max} \) and \( \omega_{min} \) minimum and maximum values of inertia weight set to be 0.4 and 0.9, respectively;
\( iter_{max} \) maximum iteration number

Figure 2 shows the flowchart of the PSO based optimal DGs planning procedure.
Figure 2 Flowchart of the PSO Based Optimal DGs Planning Procedure By velocity and position equations of PSO algorithm

5. System under evaluation

The proposed planning formulation was tested on the IEEE-13 bus feeder shown in figure (3) for which the data was obtained from IEEE test case archive for Distribution Feeders [31]. This unbalanced distribution feeder includes different system elements such as constant power, voltage and impedance loads, distributed loads, capacitors and transformers. System is operated at 4.16 kV voltage level and connected to the upstream network via a 115/4.16 kV delta-wye transformer. The total real and reactive loads of the system are 3466 MW and 2084 MVAR, respectively which are distributed on three phases.

Figure 3 IEEE 13 bus Feeder

6. Results and discussion

6.1. Cases under Evaluation

Firstly, a specific case with a definite size and site of DG is considered without solving any optimization problem from voltage quality point of view. In the next step, optimal allocation of DG is considered in order to improve system voltage
quality from a steady state lookout. Optimization problem is solved for cases of one and three DGs in power factor control mode and different coefficients of multi-objective index. Table 2 presents coefficients of MVI for every case. For cases 1 to 4, indices \( VPI, VVI, VRI \) and \( VUI \) take unity coefficient with other coefficients set at zero, respectively. Case 5 is a general voltage case which considers different aspect of voltage quality by optimizing the multi-objective index. The index coefficients of case 5 are chosen in a manner that voltage profile and unbalance take the first and second priorities, respectively and voltage regulation and variation stand in the next priority level. The tap of distribution transformer is set at 1.04 and 1 for maximum and minimum load scenarios, respectively.

Because of the inherently unbalanced nature of the IEEE 13-bus feeder, some lines and buses only consist of one or two phases which leads to large amount of unbalance in these buses. For example, bus 652 is supplied only from a single-phase feeder to support a single-phase load. Therefore, only three-phase buses are considered in \( VUI \) calculation. Moreover, in calculating \( VRI \), nominal system load and 50% of nominal load are considered as maximum and minimum load levels.

The maximum total capacity of DG is chosen 35% of system active load equal to 1200kW which leads to maximum active capacity of 400kW in each phase of the system. It is assumed that DG only injects power into present phases in the case of buses with one or two phases operated. Optimization problem is implemented and solved in MATLAB software.

**Table 2** Values of Multi-objective Index Coefficients for Different Cases.

| Case | \( \sigma_{VPI} \) | \( \sigma_{VVI} \) | \( \sigma_{VRI} \) | \( \sigma_{VUI} \) |
|------|------------------|-----------------|----------------|-----------------|
| 1    | 1                | 0               | 0              | 0               |
| 2    | 0                | 1               | 0              | 0               |
| 3    | 0                | 0               | 1              | 0               |
| 4    | 0                | 0               | 0              | 1               |
| 5    | 0.4              | 0.15            | 0.15           | 0.3             |

**6.2. A Specific Case from Voltage Quality lookout**

In this case, a DG with active power 400kW/phase and reactive power 200kVAR/phase is allocated to bus 464 and the DG output power reduction factor is set at \( f_{DG} = 0.6 \) for minimum load level scenario. The multi-objective index is calculated using coefficients of the last row of table 2. Table 3 presents the value of different indices without DG and in the presence of non-optimal DG in the system.

**Table 3** Results for a specific DG case and without DG

| Case          | \( VPI \)  | \( VVI \)  | \( VRI \)  | \( VUI \)  | \( MVI \)  |
|---------------|------------|------------|------------|------------|------------|
| With DG       | 0.8869     | 1          | 0.9782     | 0.9629     | 0.9404     |
| Without DG    | 0.8980     | 0.9797     | 0.9855     | 0.9592     | 0.9418     |

As shown in the table, indices have not improved much in the presence of DG and even \( VUI \) has worsened due to DG presence in bus 646. According to \( MVI \), system voltage quality has not got significant improvement due to DG presence. In 13-bus feeder, the least loading of the system is assigned to phase \( b \). Bus 646 only has phase \( b \) and \( c \) and DG injects power only in these phases. With the injection of this excess power, the load near DG location are supplied by DG and loading in further lines of phase \( b \) from DG is even lowered which causes more unbalance in the system. Moreover, phase \( a \) has the highest loading between phases which does not receive any generation from DG. Because of the DG active and reactive power injected in phases \( b \) and \( c \), the voltage magnitude of these phases is increased although no excess power is injected to phase \( a \) which leads to no sufficient improvement in voltage profile.

**6.3. Optimal DG allocation based on voltage Quality**

DG sitting and sizing is performed for one and three DGs allocation cases. The maximum capacity of DG is 400kW/phase. All DGs are operated in PQ mode and the power factor of DG, as one of the control variables, is set in the range of 0.85 lag to 0.85 lead.
6.3.1. One DG Allocation

Table 4 shows the optimal capacity and location of one DG in PQ mode for different cases. In the presence of DG, voltage unbalance and accordingly current unbalance is mitigated. In 13-bus feeder, the total active load of phase \( a \), \( b \) and \( c \) are 1158, 973 and 1135kW, respectively. Due to DG power injection in phases \( a \) and \( c \) and supplying some part of loads in adjacent buses such as 652 and 611 by DG, the loading of upstream lines in these phases is reduced and consequently, less current unbalance leads to less voltage unbalance.

**Table 4** Results for one DG optimal allocation in PQ mode

| Case | VPI       | VVI       | VRI       | VUI       | MVI       | \( P_{DG}/\phi \) (kW) | \( Q_{DG}/\phi \) (kW) | \( b_{DG} \) | \( f_{DG} \) |
|------|-----------|-----------|-----------|-----------|-----------|------------------------|------------------------|--------------|-------------|
| 1    | 0.9636    | 0.9704    | 0.9966    | 0.9907    | 0.9636    | 400                    | 428                    | 684          | 0.3         |
| 2    | 0.9500    | 0.9795    | 0.9952    | 0.9831    | 0.9795    | 266                    | 165                    | 684          | 0.3         |
| 3    | 0.9598    | 0.9732    | 0.9972    | 0.9885    | 0.9972    | 358                    | 222                    | 684          | 0.3         |
| 4    | 0.9636    | 0.9704    | 0.9966    | 0.9907    | 0.9907    | 400                    | 248                    | 684          | 0.3         |
| 5    | 0.9636    | 0.9704    | 0.9966    | 0.9907    | 0.9778    | 400                    | 248                    | 684          | 0.3         |

**Figure 4** Voltage profile of three phases in the presence of optimal DG

**Figure 5** Voltage profile of three phases without DG

With power injection into phases \( a \) and \( c \), the voltage drop in these phases is mitigated and voltage profile is improved. As mentioned before, with tap of transformer on 1.04, the voltage of phase \( b \) is also close to 1 pu. Therefore, with voltage of three phases close to unity, both indices of voltage profile and voltage unbalance are improved, and they are optimized in the same points. Hence, optimal DG allocations based on \( VPI \) and \( VUI \) lead to the same results. Moreover, because \( VPI \) and \( VUI \) take the highest coefficient values in case 5, the result of case 5 is also the same as cases with \( VPI \).
and $VUI$ as objective functions (cases 1 and 4). It is notable that although DG injects power only in phases $a$ and $c$, DG presence affects voltage of phase $b$. This is due to mutual impedances of lines between phases and delta connected loads.

In case two, $VVI$ is taken as the objective function. Theoretically, if the capacity of DG is zero, this index stands on unity and there is no voltage variation due to DG disconnection. However, with optimization problem limits especially those related to voltage applied, the optimal active capacity of DG is set at 294kW in bus 684 for problem limits satisfaction. In fact, DG power is chosen in a manner that $VP1$ equals 0.95 which is the minimum requisite for voltage limits satisfaction. Therefore, in all DG allocation cases, $VVI$ is not much effective and changes according to steady state voltage limits. In all cases, $VRI$ is set near unity and its variation range is not significant for different cases. This is because of considering the DG output power reduction factor ($f_{oc}$) in control variables so that the index gets proper values by setting $f_{oc}$ for low load periods.

To get a better vision of DG optimal planning, the voltage profiles of system phases for case five in the presence of DG and without DG are presented in Figure 4 and Figure 5, respectively. If one phase does not exist for a bus, the voltage of the absent phase is set at zero. As seen from figures, the three-phase voltage profile has got close to unity and has been improved by the presence of DG. By reduction of differences between phase voltage magnitudes, voltage unbalance is also mitigated, somehow. It is notable that although optimal DG only injects power into phases $a$ and $c$, voltage of phase $b$ is also reduced and closer to 1pu in the presence of DG. This is caused by phase $a$ current reduction due to DG power injection. The current of phase $a$ lags voltage of phase $a$ in most buses but this current leads voltage of phase $b$. With voltage of phase $b$ as the reference, this leading current causes voltage increase in phase $b$ due to the mutual impedance between phases. In the absence of DG, the loading and accordingly the current of phase $a$ is higher and this current decreases noticeably in the presence of DG. Therefore, voltage of phase $b$ decreases in the presence of DG and get closer to unity.

**Table 5** Results for Three DGs Optimal allocation in PQ mode

| Case | VPI   | VVI  | VRI  | VUI  | MVI  | $P_{DG}/\varphi$ (kW) | $Q_{DG}/\varphi$ (kW) | $b_{DG}$ | $f_{DG}$ |
|------|-------|------|------|------|------|------------------------|------------------------|----------|----------|
| 1    | 0.9650| 0.9797| 0.9935| 0.9786| 0.9650| 137                    | 85                     | 684      | 0.3      |
|      |       |      |      |      |      | 215                    | 134                    | 671      | 1        |
|      |       |      |      |      |      | 47                     | 29                     | 692      | .51      |
| 2    | 0.9500| 0.9941| 0.9946| 0.9760| 0.9941| 127.5                  | 34                     | 684      | .38      |
|      |       |      |      |      |      | 116                    | 40                     | 671      | .4       |
|      |       |      |      |      |      | 127                    | 79                     | 692      | .56      |
| 3    | 0.9601| 0.9761| .9973| 0.9870| 0.9973| 41                     | 22                     | 680      | .3       |
|      |       |      |      |      |      | 320                    | 199                    | 675      | .3       |
|      |       |      |      |      |      | 28                     | -6                     | 692      | .3       |
| 4    | 0.9620| 0.9714| 0.9940| 0.9907| 0.9908| 386                    | 239                    | 684      | .64      |
|      |       |      |      |      |      | 13                     | 8                      | 611      | .36      |
|      |       |      |      |      |      | -                      | -                      | -        | -        |
| 5    | 0.9638| 0.9834| 0.9972| 0.9880| 0.9790| 337                    | 208                    | 684      | .3       |
|      |       |      |      |      |      | 63                     | 39                     | 671      | .66      |
|      |       |      |      |      |      | -                      | -                      | -        | -        |

### 6.3.2. Three DGs allocation

Table 5 shows the optimal results for three DGs allocation in PQ mode. In all cases, DG active capacity is set at maximum. In case 1 which is based on $VPI$, one-third of total capacity of DG is allocated to bus 684 and two-third of DG capacity is allocated to buses 692 and 671 which are connected to each other via a switch and are equipotential. It is notable that switch control strategy is not considered in planning program of DG and the switch is assumed closed, permanently. In IEEE 13-bus feeder, the power consumptions of phases $a$ and $c$ are approximately 200kW more than power consumption of phase $b$. As seen from optimal planning result of case 1, 137 kW of DG power is also injected only in phase $a$ and $c$ and the rest of DG power is allocated to buses 671 and 692 which have three phases under operation. $VPI$ get a little improvement in three DGs scenario than on DG.
In case 2, because the disconnection of the largest DG is considered, the program has chosen the DG capacity values close to each other. Moreover, the largest DG is allocated to bus 684 and injects the lowest power to the system so that its influence on voltage magnitudes is kept to the minimum and the two smaller DGs are responsible for the voltage limits satisfaction. The optimal value of VRI in different cases does not vary much due to optimal setting of floc and the variation range of this index is small. The results obtained for case 4, is similar to one DG scenario and the major portion of DG is allocated to bus 684. For three DG allocation in case 5, the results are similar to one DG scenario. In this case, by installing 60 kW DG in bus 671 and the rest in bus 684, VRI and VVI have taken a little bit more improvement which leads to more improvement in MVI. Accordingly, the system voltage quality is a little bit improved in three DG case than one DG.

7. Conclusion

In this paper, the system voltage quality in the presence of DG was evaluated and a methodology was proposed which could be used as an intermediate stage in DG planning programs or as the objective function of DG planning in systems with voltage quality priorities that are system with valuable and high-sensitive loads. The voltage quality factors including steady state voltage profile, voltage variation due to DG disconnection, voltage regulation between high and low load period and voltage unbalance were considered and DG siting and sizing were carried out based on proposed indices of voltage quality. The following conclusions could be taken from this study:

- DGs, if not properly planned and operated, not only do not improve voltage quality but also reduce voltage quality from some phenomena outlook. Or the obtained improvement may not be economical. Therefore, detailed technical and economic evaluation of DG allocation prior to installation seems necessary.
- DGs could improve system voltage profile, but the overvoltage caused in low load periods can limit DG capacity in the system. By including DG scheduling in planning (loading factor), this problem is handled somewhat.
- DGs, if properly planned, can mitigate current unbalance and consequently voltage unbalance, by balancing loading of system lines.
- Multi-objective voltage index (MVI) is a useful tool in evaluating system voltage quality which could be used in voltage quality investigation of an operated system or in DG planning and technical comparison between several economical scenarios of DG allocation.

Compliance with ethical standards

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