Cross-Domain Object Matching with Model Selection

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Abstract

The goal of cross-domain object matching (CDOM) is to find correspondence between two sets of objects in different domains in an unsupervised way. Photo album summarization is a typical application of CDOM, where photos are automatically aligned into a designed frame expressed in the Cartesian coordinate system. CDOM is usually formulated as finding a mapping from objects in one domain (photos) to objects in the other domain (frame) so that the pairwise dependency is maximized. A state-of-the-art CDOM method employs a kernel-based dependence measure, but it has a drawback that the kernel parameter needs to be determined manually. In this paper, we propose alternative CDOM methods that can naturally address the model selection problem. Through experiments on image matching, unpaired voice conversion, and photo album summarization tasks, the effectiveness of the proposed methods is demonstrated.

1 Introduction

The objective of cross-domain object matching (CDOM) is to match two sets of objects in different domains. For instance, in photo album summarization, photos are automatically assigned into a designed frame expressed in the Cartesian coordinate system. A typical approach of CDOM is to find a mapping from objects in one domain (photos) to objects in the other domain (frame) so that the pairwise dependency is maximized. In this scenario, accurately evaluating the dependence between objects is a key challenge.

Kernelized sorting (KS) [Jebara, 2004] tries to find a mapping between two domains that maximizes the mutual information (MI) [Cover and Thomas, 2006] under the Gaussian assumption. However, since the Gaussian assumption may not be fulfilled in practice, this method (which we refer to as KS-MI) tends to perform poorly.

To overcome the limitation of KS-MI, Quadrianto et al. [2010] proposed using the kernel-based dependence measure called the Hilbert-Schmidt independence criterion (HSIC) [Gretton et al., 2005] for KS. Since HSIC is distribution-free, KS with HSIC (which we refer to as KS-HSIC) is more flexible than KS-MI. However, HSIC includes a tuning parameter (more specifically, the Gaussian kernel width), and its choice is crucial to obtain better performance (see also Jagarlamudi et al., 2010). Although using the median distance between sample points as the Gaussian kernel width is a common heuristic in kernel-based dependence measures (see e.g., Fukumizu et al., 2009a), this does not always perform well in practice.

In this paper, we propose two alternative CDOM methods that can naturally address the model selection problem. The first method employs another kernel-based dependence measure based on the normalized cross-covariance operator (NOCCO) [Fukumizu et al., 2009b], which we refer to as KS-NOCCO. The NOCCO-based dependence measure was shown to be asymptotically independent of the choice of kernels. Thus, KS-NOCCO is expected to be less sensitive to the kernel parameter choice, which is an advantage over HSIC.

The second method uses least-squares mutual information (LSMI) [Suzuki et al., 2009] as the dependence measure, which is a consistent estimator of the squared-loss mutual information (SMI) achieving the optimal convergence rate. We call this method least-squares object matching (LSOM). An advantage of LSOM is that cross-validation (CV) with respect to the LSMI criterion is possible. Thus, all the tuning parameters such as the Gaussian kernel width and the regularization parameter can be objectively determined by
CV.

Through experiments on image matching, unpaired voice conversion, and photo album summarization tasks, LSOM is shown to be the most promising approach to CDOM.

2 Problem Formulation

In this section, we formulate the problem of cross-domain object matching (CDOM).

The goal of CDOM is, given two sets of samples of the same size, \( \{x_i\}_{i=1}^n \) and \( \{y_i\}_{i=1}^n \), to find a mapping that well “matches” them.

Let \( \pi \) be a permutation function over \( \{1, \ldots, n\} \), and let \( \Pi \) be the corresponding permutation indicator matrix, i.e.,

\[
\Pi \in \{0, 1\}^{n \times n}, \quad \Pi 1_n = 1_n, \quad \text{and} \quad \Pi^\top 1_n = 1_n,
\]

where \( 1_n \) is the \( n \)-dimensional vector with all ones and \( ^\top \) denotes the transpose. Let us denote the samples matched by a permutation \( \pi \) by

\[
Z(\Pi) := \{(x_i, y_{\pi(i)})\}_{i=1}^n.
\]

The optimal permutation, denoted by \( \Pi^* \), can be obtained as the maximizer of the dependency between the two sets \( \{x_i\}_{i=1}^n \) and \( \{y_i\}_{i=1}^n \):

\[
\Pi^* := \arg\max_{\Pi} D(Z(\Pi)),
\]

where \( D \) is some dependence measure.

3 Existing Methods

In this section, we review two existing methods for CDOM, and point out their weaknesses.

3.1 Kernelized Sorting with Mutual Information

Kernelized sorting with mutual information (KS-MI) (Jebara, 2004) matches objects in different domains so that MI between matched pairs is maximized. Here, we review KS-MI following alternative derivation provided in Quadranto et al. (2010).

MI is one of the popular dependence measures between random variables. For random variables \( X \) and \( Y \), MI is defined as follows (Cover and Thomas, 2006):

\[
\text{MI}(Z) := \int p(X, Y) \log \frac{p(X, Y)}{p(X)p(Y)} \, dX \, dY,
\]

where \( p(X, Y) \) denotes the joint density of \( X \) and \( Y \), and \( p(X) \) and \( p(Y) \) are marginal densities of \( X \) and \( Y \), respectively. MI is zero if and only if \( X \) and \( Y \) are independent, and thus it may be used as a dependency measure. Let \( H(X), H(Y), \) and \( H(X, Y) \) be the entropies of \( X \) and \( Y \) and the joint entropy of \( X \) and \( Y \), respectively:

\[
H(X) = -\int p(X) \log p(X) \, dX,
\]

\[
H(Y) = -\int p(Y) \log p(Y) \, dY,
\]

\[
H(X, Y) = -\int p(X, Y) \log p(X, Y) \, dX \, dY,
\]

respectively. Then the mutual information between \( X \) and \( Y \) can be written as

\[
\text{MI}(Z) = H(X) + H(Y) - H(X, Y).
\]

Since \( H(X) \) and \( H(Y) \) are independent of permutation \( \Pi \), maximizing mutual information is equivalent to minimizing the joint entropy \( H(X, Y) \).

If \( p(X, Y) \) is Gaussian with covariance matrix \( \Sigma \), the joint entropy is expressed as

\[
H(X, Y) = \frac{1}{2} \log |\Sigma| + \text{Const},
\]

where \( |\Sigma| \) denotes the determinant of matrix \( \Sigma \).

Now, let us assume that \( x \) and \( y \) are jointly normal in some reproducing Kernel Hilbert Spaces (RKHSs) endowed with joint kernel \( K(x, x')L(y, y') \), where \( K(x, x') \) and \( L(y, y') \) are reproducing kernels for \( x \) and \( y \), respectively. Then KS-MI is formulated as follows:

\[
\min_{\Pi} \log \left| \Gamma(K \odot (\Pi^\top L \Pi)) \Gamma \right|,
\]

where \( K = \{K(x_i, x_j)\}_{i,j=1}^n \) and \( L = \{L(y_i, y_j)\}_{i,j=1}^n \) are kernel matrices, \( \odot \) denotes the Hadamard product (a.k.a. the element-wise product), \( \Gamma = I_n - \frac{1}{n} 1_n 1_n^\top \) is the centering matrix, and \( I_n \) is the \( n \)-dimensional identity matrix.

A critical weakness of KS-MI is the Gaussian assumption, which may not be fulfilled in practice.

3.2 Kernelized Sorting with Hilbert-Schmidt Independence Criterion

Kernelized sorting with Hilbert-Schmidt independence criterion (KS-HSIC) matches objects in different domains so that HSIC between matched pairs is maximized.

HSIC is a kernel-based dependence measure given as follows (Gretton et al., 2005):

\[
\text{HSIC}(Z) = \text{tr}(K L),
\]
where $\tilde{K} = \Gamma K \Gamma$ and $\tilde{L} = \Gamma L \Gamma$ are the centered kernel matrices for $x$ and $y$, respectively. Note that smaller HSIC scores mean that $X$ and $Y$ are closer to be independent.

KS-HSIC is formulated as follows (Quadrianto et al., 2010):

$$\max_{\Pi} \text{HSIC}(Z(\Pi)), \quad (2)$$

where

$$\text{HSIC}(Z(\Pi)) = \text{tr}(\tilde{K} \Pi^\top \tilde{L} \Pi). \quad (3)$$

This optimization problem is called the quadratic assignment problem (QAP) (Kuhn, 1955), and it is known to be NP-hard. There exists several QAP solvers such as methods based on simulated annealing, tabu search, and genetic algorithms. However, those QAP solvers are not easy to use in practice since they contain various tuning parameters.

Another approach to solving Eq.(2) based on a linear assignment problem (LAP) (Kuhn, 1955) was proposed in Quadrianto et al. (2010), which is explained below. Let us relax the permutation indicator matrix $\Pi$ to take real values:

$$\Pi \in [0, 1]^{n \times n}, \quad \Pi_{1n} = 1_n, \quad \text{and} \quad \Pi^\top 1_n = 1_n. \quad (4)$$

Then, Eq.(3) is convex with respect to $\Pi$ (see Lemma 7 in Quadrianto et al., 2010), and its lower bound can be obtained using some $\tilde{\Pi}$ as follows:

$$\text{tr}(\tilde{K} \Pi^\top \tilde{L} \Pi) \geq \text{tr}(\tilde{K} \tilde{\Pi}^\top \tilde{L} \tilde{\Pi}) + (\Pi - \tilde{\Pi}, \frac{\partial \text{HSIC}(Z(\Pi))}{\partial \Pi})$$

$$= 2\text{tr}(\tilde{K} \tilde{\Pi}^\top \tilde{L} \tilde{\Pi}) - \text{tr}(\tilde{K} \tilde{\Pi}^\top \tilde{L} \tilde{\Pi}), \quad (5)$$

where $\langle \cdot, \cdot \rangle$ denotes the inner product between matrices. Based on the above lower bound, Quadrianto et al. (2010) proposed to update the permutation matrix as

$$\Pi^{\text{new}} = (1 - \eta)\Pi^{\text{old}} + \eta \arg\max_{\Pi} \text{tr}(\Pi^\top \tilde{L} \Pi^{\text{old}} \tilde{K}), \quad (5)$$

where $0 < \eta \leq 1$ is a step size. The second term is an LAP subproblem, which can be efficiently solved by using the Hungarian method.

In the original KS-HSIC paper (Quadrianto et al., 2010), a C++ implementation of the Hungarian method provided by Cooper was used for solving Eq.(5); then $\Pi$ is kept updated by Eq.(5) until convergence.

In this iterative optimization procedure, the choice of initial permutation matrices is critical to obtain a good solution. Quadrianto et al. (2010) proposed the following initialization scheme. Suppose the kernel matrices $K$ and $\tilde{L}$ are rank one, i.e., for some $f$ and $g$, $K$ and $\tilde{L}$ can be expressed as $K = ff^\top$ and $\tilde{L} = gg^\top$. Then HSIC can be written as

$$\text{HSIC}(Z(\Pi)) = ||f^\top \Pi g||^2. \quad (6)$$

The initial permutation matrix is determined so that Eq.(6) is maximized. According to Theorems 368 and 369 in Hardy et al. (1952), the maximum of Eq.(6) is attained when the elements of $f$ and $\Pi g$ are ordered in the same way. That is, if the elements of $f$ are ordered in the ascending manner (i.e., $f_1 \leq f_2 \leq \cdots \leq f_n$), the maximum of Eq.(6) is attained by ordering the elements of $g$ in the same ascending way. However, since the kernel matrices $K$ and $\tilde{L}$ may not be rank one in practice, the principal eigenvectors of $K$ and $\tilde{L}$ were used as $f$ and $g$ in the original KS-HSIC paper (Quadrianto et al., 2010). We call this eigenvalue-based initialization.

Since HSIC is a distribution-free dependence measure, KS-HSIC is more flexible than KS-MI. However, a critical weakness of HSIC is that its performance is sensitive to the choice of kernels (Jagarlamudi et al., 2009b). A practical heuristic is to use the Gaussian kernel with the same way. That is, if the elements of $f$ and $g$ in the ascending manner (i.e., $f_1 \leq f_2 \leq \cdots \leq f_n$), the maximum of Eq.(6) is attained by ordering the elements of $g$ in the same ascending way. However, since the kernel matrices $K$ and $\tilde{L}$ may not be rank one in practice, the principal eigenvectors of $K$ and $\tilde{L}$ were used as $f$ and $g$ in the original KS-HSIC paper (Quadrianto et al., 2010). We call this eigenvalue-based initialization.

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4 Proposed Methods

In this section, we propose two alternative CDOM methods that can naturally address the model selection problem.

4.1 Kernelized Sorting with Normalized Cross-Covariance Operator

The kernel-based dependence measure based on the normalized cross-covariance operator (NOCCO) (Fukumizu et al., 2009b) is given as follows (Fukumizu et al., 2009a):

$$D_{\text{NOCCO}}(Z) = \text{tr}(\tilde{K} \tilde{L}),$$

where $\tilde{K} = K(K + n\epsilon I_n)^{-1}$, $\tilde{L} = L(L + n\epsilon I_n)^{-1}$, and $\epsilon > 0$ is a regularization parameter. $D_{\text{NOCCO}}$ was shown to be asymptotically independent of the choice of kernels. Thus, KS with $D_{\text{NOCCO}}$ (KS-NOCCO) is expected to be less sensitive to the kernel parameter choice than KS-HSIC.
The permuted version of $\tilde{L}$ can be written as
\[
\tilde{L}(\Pi) = \Pi^\top \tilde{L} \Pi (\Pi^\top \tilde{L} \Pi + n\epsilon I_n)^{-1}
= \Pi^\top \tilde{L} (\tilde{L} + n\epsilon I_n)^{-1} \Pi
= \Pi^\top \tilde{L} \Pi,
\]
where we used the orthogonality of $\Pi$ (i.e., $\Pi^\top \Pi = \Pi \Pi^\top = I_n$). Thus, the dependency measure for $Z(\Pi)$ can be written as
\[
D_{\text{NOCCO}}(Z(\Pi)) = \text{tr}(\tilde{K} \Pi^\top \tilde{L} \Pi).
\]
Since this is essentially the same form as HSIC, a local optimal solution may be obtained in the same way as KS-HSIC:
\[
\Pi^{\text{new}} = (1 - \eta)\Pi^{\text{old}} + \eta \arg\max_{\Pi} \text{tr} \left( \Pi^\top \tilde{L} \Pi^{\text{old}} \tilde{K} \right).
\]
(7)

However, the property that $D_{\text{NOCCO}}$ is independent of the kernel choice holds only asymptotically. Thus, with finite samples, $D_{\text{NOCCO}}$ does depend on the choice of kernels as well as the regularization parameter $\epsilon$ which needs to be manually tuned.

### 4.2 Least-Squares Object Matching

Next, we propose an alternative method called least-squares object matching (LSOM), in which we employ least-squares mutual information (LSMI) (Suzuki et al., 2009) as a dependency measure. LSMI is a consistent estimator of the squared-loss mutual information (SMI) achieving the optimal convergence rate. SMI is defined and expressed as
\[
\text{SMI}(Z) = \frac{1}{2} \int \int \left( \frac{p(X,Y)}{p(X)p(Y)} - 1 \right)^2 p(X)p(Y)dXdY
= \frac{1}{2} \int \int \left( \frac{p(X,Y)}{p(X)p(Y)} \right) p(X,Y)dXdY - \frac{1}{2}. \tag{8}
\]
Note that SMI is the Pearson divergence (Pearson, 1900) from $p(X,Y)$ to $p(X)p(Y)$, while ordinary MI is the Kullback-Leibler divergence (Kullback and Leibler, 1951) from $p(X,Y)$ to $p(X)p(Y)$. SMI is zero if and only if $X$ and $Y$ are independent, as ordinary MI. Its estimator LSMI is given as follows (Suzuki et al., 2009):
\[
\text{LSMI}(Z) = \frac{1}{2} \alpha^\top h - \frac{1}{2},
\]
where
\[
\alpha = H^{-1}h,
\]
\[
H = \frac{1}{\eta^2} \left( (KK^\top) \circ (LL^\top) + \lambda I_n \right),
\]
\[
h = \left( \frac{1}{n} K \circ L \right) 1_n.
\]
Here, $\lambda (\geq 0)$ is the regularization parameter. Since cross-validation (CV) with respect to SMI is possible for model selection, tuning parameters in LSMI (i.e., the Gaussian kernel width and the regularization parameter) can be objectively optimized. This is a notable advantage over kernel-based approaches.

Below, we use the following equivalent expression of LSMI:
\[
\text{LSMI}(Z) = \frac{1}{2n} \text{tr} \left( LAK \right) - \frac{1}{2}. \tag{9}
\]
where $A$ is the diagonal matrix with diagonal elements given by $\alpha$. Note that we used Eq.(73) and Eq.(75) in Minka (2000) for obtaining the above expression. LSMI for the permuted data $Z(\Pi)$ is given by
\[
\text{LSMI}(Z(\Pi)) = \frac{1}{2n} \text{tr} \left( \Pi^\top L \Pi A_{\Pi} K \right) - \frac{1}{2},
\]
where $A_{\Pi}$ is the diagonal matrix with diagonal elements given by $\alpha_{\Pi}$, and $\alpha_{\Pi}$ is given by
\[
\alpha_{\Pi} = H_{\Pi}^{-1}h_{\Pi},
\]
\[
H_{\Pi} = \frac{1}{\eta^2} \left( (KK^\top) \circ (LL^\top) + \lambda I_n \right),
\]
\[
h_{\Pi} = \left( \frac{1}{n} K \circ (LL^\top) \right) 1_n.
\]
Consequently, LSOM is formulated as follows:
\[
\max_{\Pi} \text{LSMI}(Z(\Pi)).
\]
Since this optimization problem is in general NP-hard and is not convex, we simply use the same optimization strategy as KS-HSIC, i.e., for the current $\Pi^{\text{old}}$, the solution is updated as
\[
\Pi^{\text{new}} = (1 - \eta)\Pi^{\text{old}} + \eta \arg\max_{\Pi} \text{tr} \left( \Pi^\top L \Pi^{\text{old}} A_{\Pi^{\text{old}}} K \right). \tag{10}
\]

### 5 Experiments

In this section, we first illustrate the behavior of the proposed methods using a toy data set, and then experimentally evaluate our proposed algorithms in the image matching, unpaired voice conversion, and photo album summarization tasks.

In all the methods, we use the Gaussian kernels:
\[
K(x, x') = \exp \left( -\frac{||x - x'||^2}{2\sigma_x^2} \right),
\]
\[
L(y, y') = \exp \left( -\frac{||y - y'||^2}{2\sigma_y^2} \right),
\]
and we set the maximum number of iterations for updating permutation matrices to 20 and the step size $\eta$ to 1. To avoid falling into undesirable local optima, optimization is carried out 10 times with different initial permutation matrices, which are determined by the eigenvalue-based initialization heuristic with Gaussian kernel widths $(\sigma_x, \sigma_y) = c \times (m_x, m_y)$, where $c = 1^{1/2}, 2^{1/2}, \ldots, 10^{1/2}$, and

\[
\begin{align*}
& m_x = 2^{-1/2}\text{median}(\{||x_i - x_j||\}_{i,j=1}^n), \\
& m_y = 2^{-1/2}\text{median}(\{||y_i - y_j||\}_{i,j=1}^n).
\end{align*}
\]

In KS-HSIC and KS-NOCCO, we use the Gaussian kernel with the following widths:

\[
(\sigma_x, \sigma_y) = c' \times (m_x, m_y),
\]

where $c' = 1^{1/2}, 10^{1/2}$. In KS-NOCCO, we use the following regularizer parameters:

\[
\epsilon = 0.01, 0.05.
\]

In LSOM, we choose the model parameters of LSMI, $\sigma_x$, $\sigma_y$, and $\lambda$ by 2-fold CV from

\[
(\sigma_x, \sigma_y) = c \times (m_x, m_y), \\
\lambda = 10^{-1}, 10^{-2}, 10^{-3}.
\]

5.1 Illustrative Example

Here, we illustrate the behavior of the proposed KS-NOCCO and LSOM using a toy matching dataset.

Let us consider the following regression model:

\[
Y = X^3,
\]

where $X$ is subject to the uniform distribution on $(-1, 1)$. We draw 100 paired samples of $X$ and $Y$ following the above generative model (i.e., $\{(x_i, y_i)\}_{i=1}^{100}$). Then, given that $\{y_i\}_{i=1}^{100}$ are randomly shuffled, the goal is to recover the original correspondence. In KS-NOCCO, we set the Gaussian kernel width to

\[
(\sigma_x, \sigma_y) = 10^{1/2} \times (m_x, m_y),
\]

and $\epsilon = 0.05$.

Figure 1(a) shows the original unpaired data, where the true function is shown by the solid line. Figure 1(b) shows the matched pairs with eigenvalue-based initialization, and Figures 1(c) and 1(d) show the matched pairs by KS-NOCCO and LSOM. The graphs show that matching are performed correctly by KS-NOCCO and LSOM. Figures 1(e) and 1(f) show the values of $D_{\text{NOCCO}}$ and LSMI scores as functions of the number of iterations. This shows that a local optimal solution has been obtained only in one iteration.
Next, let us consider a toy image matching problem: we vertically divide images of size $40 \times 40$ pixels in the middle, and make two sets of half-images $\{x_i\}_{i=1}^n$ and $\{y_i\}_{i=1}^n$. Given that $\{y_i\}_{i=1}^n$ is randomly permuted, the goal is to recover the correct correspondence.

Figure 2 summarizes the average correct matching rate over 100 runs as functions of the number of images, showing that the proposed LSOM method tends to outperform the best tuned KS-NOCCO and KS-HSIC methods. Figure 3 depicts an example of image matching results obtained by LSOM, showing that most of the images are matched correctly.

5.3 Unpaired Voice Conversion

Next, we consider an unpaired voice conversion task, which is aimed at matching the voice of a source speaker with that of a target speaker.

In this experiment, we use 200 short utterance samples recorded from two male speakers in French, with sampling rate 44.1kHz. We first convert the utterance samples to 50-dimensional line spectral frequencies (LSF) vector. We denote the source and target LSF vectors by $x$ and $y$, respectively. Then the voice conversion task can be regarded as a multi-dimensional regression problem of learning a function from $x$ to $y$. However, different from a standard regression setup, paired training samples are not available; instead, only unpaired samples $\{x_i\}_{i=1}^n$ and $\{y_i\}_{i=1}^n$ are given.

By CDOM, we first match $\{x_i\}_{i=1}^n$ and $\{y_i\}_{i=1}^n$, and then we train a multi-dimensional kernel regression model using the matched samples $\{(x_{\pi(i)}, y_i)\}_{i=1}^n$ as

$$\min_W \sum_{i=1}^n \|y_i - W^T k(x_{\pi(i)})\|^2 + \frac{\delta}{2} \text{tr}(W^T W),$$

where

$$k(x) = (K(x, x_{\pi(1)}), \ldots, K(x, x_{\pi(n)}))^T,$$

$$K(x, x') = \exp\left(-\frac{\|x - x'\|^2}{2\tau^2}\right).$$

Here, $\tau$ is a Gaussian kernel width and $\delta$ is a regularization parameter; they are chosen by 2-fold CV.

We repeat the experiments 100 times by randomly shuffling training and test samples, and evaluate the voice conversion performance by log-spectral distance for 8000 test samples. Figure 4 shows the true spectral envelope and their estimates, and Figure 5 shows the average performance.

Figure 2: Image matching results. The best method in terms of the mean error and comparable methods according to the t-test at the significance level 1% are specified by ‘*’.  

Figure 3: Image matching result by LSOM. In this case, 234 out of 320 images (73.1%) are matched correctly. 

The smaller the spectral distortion is, the better the quality of voice conversion is.
Figure 4: True spectral envelopes and their estimates.

Figure 5: Unpaired voice conversion results. The best method in terms of the mean error and comparable methods according to the t-test at the significance level 1% are specified by '◦'.

over 100 runs as the number of training samples. These results show that the proposed LSOM tends to outperform KS-NOCCO and KS-HSIC.

5.4 Photo Album Summarization

Finally, we apply the proposed LSOM method to a photo album summarization problem, where photos are automatically aligned into a designed frame expressed in the Cartesian coordinate system.

We use 320 images with RGB format used in Quadrianto et al. (2010), which were originally extracted from Flickr. We first convert the images from RGB to Lab space and resize them to 40 × 40 pixels. Next, we convert a 40 × 40 × 3 (= 4800) image into a 4800-dimensional vector. We first consider a rectangular frame of 16 × 20 (= 320), and arrange the images in this rectangular frame. Figure 6(a) depicts the photo album summarization result, showing that images are aligned in the way that images with similar colors are aligned closely.

Similarly, we use the Frey face dataset (Roweis and Saul, 2000), which consists of 225 gray-scale face images with 28 × 20 (= 560) pixels. We similarly convert a image into a 560-dimensional vector, and we set the grid size to 15 × 15 (= 225). The results depicted in Figure 6(b) shows that similar face images (in terms of the angle and facial expressions) are assigned in nearby cells in the grid.

Next, we apply LSOM to the USPS dataset (Hastie et al., 2001). In this experiment, we use 320 gray-scale images of digit ‘7’ with 16 × 16 (= 256) pixels. We convert an image into a 256-dimensional vector, and we set the grid size to 16 × 20 (= 320). The result depicted in Figure 6(c) shows that digits with similar profiles are aligned closely.

Finally, we align the Flickr, Frey face, and USPS images into more complex frames—a Japanese character ‘mountain’, a smiley-face shape, and a ‘777’ digit shape. The results depicted in Figure 7 shows that images with similar profiles are located in nearby grid coordinate cells.

6 Conclusion

In this paper, we proposed two alternative methods of cross-domain object matching (CDOM). The first method uses the dependence measure based on the normalized cross-covariance operator, which is advantageous over HSIC in that it is asymptotically independent of the choice of kernels. However, with finite samples, it still depends on the choice of kernels which needs to be manually tuned. To cope with this problem, we proposed a more practical CDOM approach called least-squares object matching (LSOM). LSOM adopts squared-loss mutual information as a dependence measure, and it is estimated by the method of least-squares mutual information (LSMI). A notable advantage of the LSOM method is that it is equipped
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Figure 6: Images are automatically aligned into rectangular grid frames expressed in the Cartesian coordinate system.

Figure 7: Images are automatically aligned into complex grid frames expressed in the Cartesian coordinate system.

with a natural cross-validation procedure that allows us to objectively optimize tuning parameters such as the Gaussian kernel width and the regularization parameter in a data-dependent fashion. We applied the proposed methods to the image matching, unpaired voice conversion, and the photo album summarization tasks, and experimentally showed that LSOM is the most promising.

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