Probing the electronic states and impurity effects in black phosphorus vertical heterostructures

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Keywords: black phosphorus, electronic states, quantum capacitance, vertical heterostructure, impurity

Abstract
Atomically thin black phosphorus (BP) is a promising two-dimensional material for fabricating electronic and optoelectronic nano-devices with high mobility and tunable bandgap structures. However, the charge-carrier mobility in few-layer phosphorene (monolayer BP) is mainly limited by the presence of impurity and disorders. In this study, we demonstrate that vertical BP heterostructure devices offer great advantages in probing the electron states of monolayer and few-layer phosphorene at temperatures down to 2 K through capacitance spectroscopy. Electronic states in the conduction and valence bands of phosphorene are accessible over a wide range of temperature and frequency. Exponential band tails have been determined to be related to disorders. Unusual phenomena such as the large temperature-dependence of the electron state population in few-layer phosphorene have been observed and systematically studied. By combining the first-principles calculation, we identified that the thermal excitation of charge trap states and oxidation-induced defect states were the main reasons for this large temperature dependence of the electron state population and degradation of the on-off ratio in phosphorene field-effect transistors.

Atomically thin black phosphorus (BP), a two-dimensional (2D) layered material held together by van der Waals interactions, has attracted great attention recently owing to its unique properties [1–12]. Few-layer phosphorene normally has high charge-carrier mobility [1, 9, 10, 12] (~1000 cm^2 V^{-1} s^{-1}) in comparison with transition metal dichalcogenides at room temperature [13–16]. The strong ambipolar field effects [1–3, 17, 18] and tunable bandgap [17–22] observed in phosphorene allow the realization of electrically tunable PN junctions [5], heterojunctions [23] and high-performance radio-frequency transistors [24]. Thanks to its small and direct bandgap [19, 20], few-layer phosphorene also shows fast photoresponse and broad-band energy harvesting up to the near-infrared [4, 5, 25] range.

To further boost up the applications of BP, its charge-carrier mobility needs to be optimized. Unfortunately, the carrier mobility of atomically thin BP is still much lower than the theoretically predicted value (~10 000 cm^2 V^{-1} s^{-1} [26]) due to the presence of impurity and disorders. The preparation of monolayer and few-layer phosphorene (thickness <2 nm) is still challenging because phosphorene is easily oxidized in the atmosphere [1–3, 27–29]. Investigation of the electron states of atomically thin BP is important to better understand the relationship between charge carrier behavior, band structure and impurity states in BP and other types of 2D semiconductors [16, 30–32]. In this study, we demonstrate the advantages of capacitance spectroscopy techniques for investigating the electronic states in a vertical BP heterostructure (figures 1(a)–
which is different from conventional field-effect transistor (FET) devices. In conventional 2D semiconductor FET structures, charge carriers normally suffer from a large lateral resistance and electrons are often localized near the band edge, causing difficulties in detecting electronic states at low temperature and high frequency conditions [16, 30, 31]. In contrast, the electrons in the vertical configuration reported in our previously work [15] can respond directly and efficiently (figure 1(b)) without suffering the large lateral resistance near the band edge. We show that the electron states in both monolayer and few-layer phosphorene can be detected over wide ranges of temperature (2 K–300 K) and frequency (100 Hz–1 MHz). A number of interesting properties in few-layer phosphorene such as the large variation of electron state population at different temperatures, exponential band tail changes for different Fermi energies, thickness-dependent band gap width and variation of charge trap density have been observed.

As shown in figures 1(a)–(c), the vertical heterostructure consists of a thin BP flake and a hexagonal boron nitride (hBN) dielectric layer (6 nm–20 nm) sandwiched by a bottom gate (Cr/Au, 2 nm/25 nm) supported on a 300 nm SiO2/p-Si substrate and a top electrode (Ti/Au, 5 nm/50 nm). Ultrathin BP flakes were mechanically exfoliated and identified in a glove box equipped with an optical microscope in nitrogen atmosphere in order to avoid sample quality degradation. The number of layers of BP on the SiO2 substrate was confirmed by quick atomic force microscope scans before transferring to metal-BN stacks (see the supporting information). The fully covered top electrode further isolates BP flakes from oxidation when transferring the sample through air. By applying an alternating current (AC) parameterized with a frequency \( f \) and a gate voltage \( V_g \) to the vertical structure (figure 1(c)), electron states of BP are excited and contribute to the capacitance \( C_{\text{BP}} \), in a series connection with the geometric capacitance \( C_g \) (figure 1(d)). Then the measured capacitance is expressed as 

\[
C_i = \frac{1}{C_g} + \frac{1}{C_{\text{BP}}} \quad \text{after excluding the parallel residue capacitance } C_p \quad \text{(see details in the supporting information)}.
\]

Figure 2(g) illustrates the capacitance data measured as a function of gate voltage for a 7.2 nm-thick BP sample at 2 K. The strong ambipolar capacitance behavior indicates that both hole and electron doping states have been achieved. The top electrode has an excellent Ohmic contact with the valence band of the BP sample and the Schottky barrier to the conduction band is overcome when the excitation voltage (\( \gtrsim 100 \text{ meV} \)) is applied at 100 kHz (see the inset of figure 2(g)). Note that the notion of the Schottky barrier should not be applied to monolayer BP because of the lack of the depletion region in the monolayer limit. The band diagrams should be described by energy level diagrams (figures 2(d)–(f)). When the gate voltage is reversed to be negative, holes start to accumulate at the BP surface (figure 2(a)), while electrons

(c)
form at the interface when the gate voltage $V_g > 0$ (figure 2(c)). In both cases, if $|V_g|$ is sufficiently large, the measured capacitance would approach the geometric capacitance $C_g$ (denoted by the blue dashed line in figure 2(g)). When the carriers are depleted (figure 2(b)), the measured capacitance reaches the minimum value $C_{\text{min}} = (C_g^{-1} + \frac{d_{\text{BP}}}{\varepsilon_{\text{BP}}})^{-1}$, where $\varepsilon_{\text{BP}}$ and $d_{\text{BP}}$ are the dielectric constant and the thickness of BP sample respectively. Inside the bandgap, however, the measured capacitance $C_{\text{BP}}$ in this vertical configuration is normally non-zero because of the bulk capacitance $C_{\text{bulk}} = \frac{\varepsilon_{\text{BP}}}{d_{\text{BP}}}$ in parallel connection with the quantum capacitance of BP $C_q$, which is known to be proportional to the density of states (DOS) $[16, 30, 33-36]$. Then the quantum capacitance $C_q$ can be approximately expressed by $C_q = C_{\text{BP}} - \frac{\varepsilon_{\text{BP}}}{d_{\text{BP}}}$. Without considering thermal effects, the DOS of the sample can be conveniently expressed by $\text{DOS} = \frac{C_q}{2T} [34-36]$. The theoretical simulation of these characteristics of the vertical structure is demonstrated in the supporting information.

For both monolayer and few-layer phosphorene samples, the electron states in valence and conduction bands are accessible through the vertical heterostructure configurations. As shown in figures 4(a)–(d), the measured capacitance generally shows a clear ambipolar behavior from room temperature down to 2 K. This allows us to directly determine the band gap width of BP at low temperatures ($\leq 30$ K) where the thermal excitation of free carriers and charge trap states are suppressed. In order to precisely determine the band gap width, the band tail (due to the presence of impurity and disorders) should be considered. The exponential characteristic of the DOS $[30]$ in our sample (excluding charge trap states $D_{\text{tr}}$) matches the band tail’s form, $\text{DOS} \propto \exp\left(\frac{(E - E_{\text{bc}})}{E_t}\right)$, where $E_{\text{bc}} \leq E \leq E_{\text{bc}}$ and $E_t$ characterizes the energy width of the band tail. $E_{\text{bc}}$ and $E_{\text{tr}}$ are the positions of the conduction and valence bands respectively.

As shown in figure 3(b), the extracted quantum capacitance ($C_q \propto \text{DOS}$) of the 6-layer BP sample fits the exponential relationship $\text{DOS} = \alpha \cdot \exp$...
with $E_F$ near the band edge, and $E_F$ can be obtained through the charge conservation relationship $E_F = e \cdot \int_{0}^{N_F} \left( 1 - \frac{C_Q}{C_T} \right) \mathrm{d}V_F$\,[16, 33–35]. The fittings (denoted by the red line in figure 3(b)) yield the bandgap size $E_{bg} = E_{bgc} - E_{bgv} = 0.68$ eV and the band tail widths $E_{bgv} = 60$ meV and 50 meV for the valence and conduction bands respectively. Here $\alpha$ is a fitting constant. To exclude the influence of charge trap states, we performed a capacitance measurement using a high excitation frequency ($\sim 100$ kHz). The sample temperature was in the range of 20 K–30 K ($kT \ll E_{bg}$) in order to generate enough thermal electrons injected into the conduction band. This guaranteed the measurement accuracy in determining $E_{bgc}$ and the band tail width of the conduction band. To obtain an accurate capacitance, the leakage current $G$ of the capacitor should be much smaller than $\omega C_T$, where $\omega$ is the angular frequency. As shown in figure S6 in the supporting information, $G$ is about two orders smaller than $\omega C_T$, which is reasonable to neglect. Another parameter that affects the accuracy of a measurement is the AC excitation voltage. If the applied excitation voltage is too large, the measured capacitance around the band tail would become flat (see figure 2(d)) and lead to an overestimated band tail width. Due to the serial connection of the geometric capacitance and the BP capacitance, the AC voltage drops on BP flakes are only around one-tenth of the total applied excitation voltages. Hence, a reasonable excitation voltage is chosen to ensure both an accurate measurement and a small noise/signal ratio.

Based on the analysis discussed above, we obtained the band gap width of monolayer (figure 3(d)) and bilayer phosphorene (figure 3(e)). Detailed analysis can be found in the supporting information. BP

Figure 3. Characterization of the band tail and bandgap width of thin BP layers. (a)–(c) Total capacitance $C_T$ (a), quantum capacitance $C_Q$ (b) and $C_{BP}$ (c) as a function of Fermi energy measured in the 6-layer BP sample at 20 K with an excitation voltage of 200 mV and a high excitation frequency of 100 kHz. The red solid line in (b) is the fitting based on DOS = $\alpha \cdot \exp \left( \frac{|E| - E_{bgc}}{E_{bgv}} \right)$.(d)–(e) $C_{BP}$ measured as a function of Fermi energy in monolayer (d) and bilayer (e) phosphorene with an excitation voltage of 400 mV. The blue dashed lines denote the positions of the conduction and valence bands of BP determined by fitting the experimental data. (f) The bandgap width of thin BP layers plotted as a function of thickness. The blue dot denotes the bandgap width of bulk BP.
exhibits a tunable bandgap from $\sim 1.4 \text{ eV}$ (monolayer) to $\sim 0.3 \text{ eV}$ (bulk) which decreases monotonically with the sample thickness (figure 3(f)). These results are consistent with theoretical predictions [2, 19, 20, 37] and experimental results measured from phosphorene FETs [17]. We noted that the measured bandgap size in our monolayer BP is smaller than previous optical results $\sim 2 \text{ eV}$ [8]. This could be due to the oxidation of BP as demonstrated in the following theoretical calculations. We further identified the band tail width ($E_1 \sim 100 \text{ meV}$) in monolayer phosphorene which is in the same order compared to that obtained in monolayer MoS$_2$ [30], indicating a high density of impurity and disorders in BP samples.

One interesting and unexpected feature we discovered in monolayer and few layer phosphorene is the significant change of the electron state population detected by capacitance measurements at different temperatures. The measured capacitance unusually increases with increasing temperature (figures 4(a)–(d)) when the Fermi energy is inside the band gap. Such a phenomenon becomes more pronounced for thick BP samples. For example, in the 6-layer sample, the gap looks almost ‘closed up’ (figures 5(b), (e)) around 150 K ($kT \sim 13 \text{ meV}$). A further increase in temperature leads to a large increase of DOS $\sim 1 \times 10^{11} \text{ eV}^{-1} \text{ cm}^{-2}$ inside the bandgap (figures 5(c), (f)). Since thermal excitation of intrinsic electron states of BP is not able to cause this obvious change of electron state population, we propose the following mechanism based on charge trapping effects to address this phenomenon in few-layer BP. The charge trapping effects [3, 38] can be detected by performing positive and negative gate sweeping experiments. When the sample temperature is higher than 200 K, a pronounced hysteresis effect is observed (see figures 5(a)–(c) and figure S5 in the supporting information). Similar to previous transport measurements [3, 38], a positive hysteresis direction is the sign of the charge trapping effect which is different from capacitive coupling to the BP [39]. At low temperatures, the hysteresis effect disappears, further supporting the charge trapping mechanism since charge traps are frozen. We believe that the charge trap states are distributed inside the bandgap until the band edges of BP (figure 5(g)). At low temperatures, charge traps are suppressed and hence a finite gap structure is observed, while at high temperatures, charge trap states significantly contribute to the measured capacitance and increase the DOS. At a sufficiently high temperature, the gap looks ‘closed up’ due to the remarkable contribution of thermally excited charge trap states. Hence, the measured DOS through quantum capacitance here is the ‘thermodynamic’ DOS that includes both intrinsic states and excited charge trap states of BP. A more accurate way to extract the DOS is to include the contribution of the thermal broaden

Figure 4. Temperature-dependent capacitance in monolayer and few layer phosphorene. (a)–(d) Capacitance $C$ measured as a function of gate voltage $V_g$ in monolayer (a), bilayer (b), trilayer (c) and 6-layer (d) phosphorene at different temperatures. The excitation voltage and frequency are 400 mV and 100 Hz for (a), 400 mV and 100 Hz for (b), 200 mV and 100 kHz for (c), and 100 mV and 100 kHz for (d) respectively.
effect by $C_q = e^2 \int_{E_t}^{E_F} DOS \cdot f(E) dE$, where $f(E)$ is the Fermi–Dirac distribution function. As most experiments are studied at low temperatures with a neglectable thermal contribution (e.g. $kT \sim 2.6$ meV at 30 K), the approximation $DOS = \frac{C_t}{e^2}$ is still accurate.

To quantitively verify the density of charge trap states $D_{tr}$, we performed capacitance measurement at low temperatures ($\sim 2$ K) with different excitation frequencies $f$. This is because the charge traps should have a relaxation time $\tau_{tr}$. At a high excitation frequency $1/f < \tau_{tr}$, the relaxation of charge trap states is suppressed, while when $1/f > \tau_{tr}$, the charge trap states are excited and contribute to the measured quantum capacitance by adding an additional parallel capacitance $e^2 \cdot D_{tr}$. Hence, the charge trap densities can be expressed by $D_{tr} = (C_{q, low} f - C_{q, high} f)/e^2$ [16]. The extracted charge trap densities in monolayer and few layer BP samples are in the range of $10^{12} - 10^{13}$ eV$^{-1}$ cm$^{-2}$ (see figures 5(h)–(j)). Because of the limitation of the frequency range (100 Hz $\sim$ 1 MHz) in our experiment, $D_{tr}$ could be underestimated. The observed large trap densities should not come from the insulating layer of hBN since hBN has been proven to be an ultra-smooth and disorder-free dielectric material without introducing charged impurities [40]. We believe that the charge traps in BP are mainly due to the impurity and disorders induced in the fabrication processes particularly from the surface degradation caused by oxygen and water moisture [29]. Previous transport results have shown that the on-off ratio in BP FETs is small at high temperatures [1–3, 41]. Obviously, the excited charge traps should contribute a lot when measuring the on-off ratio based on conventional FET device configuration. In capacitance measurements, the DOS displays obvious asymmetry in electron and hole sides near the band edges of BP. A similar feature was also reported in previous transport measurements [3] which was attributed to

Figure 5. Temperature-dependent population of electron states in BP. (a)–(c) Hysteresis of measured capacitance $C_t$ of the 6-layer BP sample at different temperatures. (d)–(f) DOS of the 6-layer BP sample at different temperatures. (g) Schematic diagram showing the distribution of charge trap states inside the bandgap and near the band edges. (h)–(i) Charge trap densities in 6-layer (h), bilayer (i) and monolayer (j) BP samples.
the difference of electron and hole injection rates. Our capacitance results indicate that a larger on-off ratio could be achieved in monolayer and bilayer phosphorene FETs at room temperature. This is because the bandgap has not been fully 'closed up' in monolayer and bilayer phosphorene at room temperature (figures 4(a), (b)).

In addition to charge trap effects, strain induced deformation could be a possible reason for the bandgap variation in few-layer BP. It is known that strain induced deformation in the direction perpendicular to the phosphorene plane could lead to a semiconductor-to-metal transition \cite{19, 37}. Theoretical calculations \cite{19, 37} predict that the compression in phosphorene can reduce the bandgap width and eventually lead to band crossings if the deformation is sufficiently large. In our vertical heterostructures, the only factor that could induce strain in BP is the thermal expansion of BP at high temperatures. However, the thermal expansion coefficient of BP \cite{42} is $\sim 13 \times 10^{-6} \text{K}^{-1}$ which causes only a very limited strain effect.

To understand the quality degradation of BP and its influence on the bandgap size under atmospheric conditions, we performed the first-principles calculation on BP bonded with oxygen (O) and hydroxide ions (OH) based on the density functional theory method using the VASP code, within the projector augmented wave method \cite{43}. The exchange and correlation effects are described by the Perdew–Burke–Ernzerhof (PBE) form of the generalized gradient

\begin{table}[h]
\centering
\begin{tabular}{|c|c|c|c|c|c|}
\hline
Structure & P-O (Å) & O-H (Å) & P-O/Plane (°) & P-O-H (°) & Band Gap (eV) \\
\hline
BP-pristine & — & — & — & — & 0.904 \\
BP-1O & 1.506 & — & 52.535 & — & 1.035 \\
BP-2O & 1.504 & — & 48.802 & — & 1.133 \\
 & 1.504 & 52.457 & \\
BP-1OH & 1.684 & 0.978 & 88.042 & 108.709 & 0.131 \\
BP-2OH & 1.630 & 0.980 & 123.337 & 113.548 & 0.410 \\
 & 1.706 & 0.975 & 89.155 & 107.833 & \\
\hline
\end{tabular}
\caption{Calculated structural parameters and bandgap of monolayer phosphorene.}
\end{table}
approximation. The Monkhorst–Pack k point-mesh is chosen to be $5 \times 1 \times 5$ for monolayer BP supercell models and the cutoff energy is set to 550 eV. The total ground state energy is converged within $10^{-6}$ eV per unit cell, and all the atoms are fully relaxed until the Hellmann–Feynman forces exerted on each atom become less than 0.01 eV Å$^{-1}$. The spin polarization has been taken into account in all of our calculations. As shown in table 1, the calculated bandgap size for pristine monolayer phosphorene is 0.904 eV, which is consistent with previous PBE results [26]. Although the PBE method might underestimate the bandgap size of BP, it provides useful information on the relative change of the bandgap of phosphorene with defects. Geometric configurations of O and OH defects of different concentrations in phosphorene are shown in figure 6. Table 1 illustrates the calculation results for such O and OH adatoms bonded on the surface of monolayer BP, including bonding lengths and bonding angles. O slightly increases the bandgap size of monolayer phosphorene, whereas OH can significantly decrease its bandgap size. Thus the oxidation effect could effectively lead to a smaller bandgap in monolayer phosphorene, through the modification of electronic properties by extrinsic point defects.

To investigate the influence of the B and N defects which possibly come from hBN in the heterostructure, we employed a $5 \times 4$ supercell containing 80 P atoms to simulate B and N defects in the BP, as illustrated in figure 7. In contrast to O absorption, for B and N adatoms (either adsorbed on the BP surface or interstitially embedded in the BP layer) spin splitting of DOS peaks near the valence band edge can be found; consequently the spin polarized charge density is localized on the atoms around the adatoms. Thus, these impurities might provide additional sources of charge trap states discovered in our experiments. As shown in figure S7 of the supporting information, four substitution doping configurations are also considered, including B, N doping and B/N co-doping with two different B-N defect distances. We found all these defects in BP generally decrease the band gap of BP. For the N defect (having the same valence as P) in BP, the band gap is reduced to 0.79 eV without a distinct mid-gap state near the conduction band. For the other defects, the band gaps decrease considerably with the appearance of middle states, as a result of hole doping owing to the B defect in the BP.

In summary, the vertical BP/hBN heterostructure configuration offers advantages in probing the

![Figure 7. Geometric configurations and calculated DOS of (a) B atom, and (b) N atom, adsorbed on the surface of monolayer phosphorene.](image-url)
electron states of monolayer and few layer phospho-

erene at temperatures down to 2 K for capacitance 
spectroscopy. Important information such as DOS, 
bandgap width and charge trap density has been 
obtained from the quantum capacitance measure-
ment. The thermal excitation of charge trap states has 
been identified to be the main reason for the large 
temperature-dependence of the electron state popu-
lation, capacitance, transport hysteresis and asymmetry 
distribution of DOS. Combined with first principles 
calculations, our experimental results show directions 
for improving the quality and on-off ratios of BP FETs.

Acknowledgment

Financial support from the Research Grants Council 
of Hong Kong (Project Nos. 16302215, HKU9/CRF/
13G, 604112 and N_HKUST613/12) and technical 
support of the Raith-HKUST Nanotechnology 
Laboratory for the electron-beam lithography facility 
at MCPF (Project No. SEG_HKUST08) are hereby 
acknowledged. This work was also supported by the 
National Key Basic Research Program of China (Grant 
No. 2015CB921600), the National Natural Science 
Foundation of China (NSFC, Grant No. 11274222), 
the QiMingXing Project (Project No. 14QA1402000) 
of the Shanghai Municipal Science and Technology 
Commission, the Eastern Scholar Program, and the 
Shuguang Program (Grant No. 12SG34) from the 
Shanghai Municipal Education Commission.

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