Time-Resolved Thickness and Shape-Change Quantification using a Dual-Band Nanoplasmonic Ruler with Sub-Nanometer Resolution

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ABSTRACT: Time-resolved measurements of changes in the size and shape of nanobiological objects and layers are crucial to understand their properties and optimize their performance. Optical sensing is particularly attractive with high throughput and sensitivity, and label-free operation. However, most state-of-the-art solutions require intricate modeling or multi-parameter measurements to disentangle conformational or thickness changes of biomolecular layers from complex interfacial refractive index variations. Here, we present a dual-band nanoplasmonic ruler comprising mixed arrays of plasmonic nanoparticles with spectrally separated resonance peaks. As electrodynamic simulations and model experiments show, the ruler enables real-time simultaneous measurements of thickness and refractive index variations in uniform and heterogeneous layers with sub-nanometer resolution. Additionally, nanostructure shape changes can be tracked, as demonstrated by quantifying the degree of lipid vesicle deformation at the critical coverage prior to rupture and supported lipid bilayer formation. In a broader context, the presented nanofabrication approach constitutes a generic route for multimodal nanoplasmonic optical sensing.

KEYWORDS: biomolecules, biosensors, conformation, nanoplasmonic sensors, nanorulers, supported lipid bilayer

The ability to accurately measure the size and shape of nanoscale objects is one of the key achievements of nanoscience and nanotechnology, since these characteristics dictate many properties and functionalities of nanoscale objects in materials and life science. In the latter area, precise characterization of nanoscopic biological entities is especially important, e.g., for the development of advanced diagnostics and therapeutic systems and tools, since many diseases are induced by a modified functionality of such entities due to changes in their structure or conformation. For example, protein misfolding and amyloid fibril formation is associated with Alzheimer’s disease and an increased size of saliva and urinary exosomes is correlated with the occurrence of oral and prostate cancers, respectively. On the other hand, the size of lipid nanoparticles and exosomes is also a critical parameter for their efficiency in drug delivery. At the same time, performing an accurate size and shape determination of nanoscopic biological entities is challenging because they are “soft” and highly dynamic and because their dimensions and conformation depend on interactions with other biological species or surfaces in their surroundings. To this end, various techniques have been used to quantify such systems, including transmission electron microscopy (TEM), X-ray crystallography, neutron reflectometry, and nuclear magnetic resonance (NMR). However, TEM seldomly enables characterization of the dynamics of such processes and thus

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prohibits studies of conformational change in real time.\textsuperscript{19,20} This situation is similar to X-ray crystallography due to its requirement of crystalline samples. In contrast, both neutron reflectometry and NMR permit the study of conformational dynamics, however, only with low throughput and high sample consumption.\textsuperscript{15–18}

In this regard, optical sensing techniques, such as ellipsometry,\textsuperscript{21} silicon microring resonators (SMR),\textsuperscript{22,23} optical waveguide lighmode spectroscopy (OWLS),\textsuperscript{24,25} and surface plasmon resonance (SPR),\textsuperscript{26–28} are attractive tools since they provide sensitive, label-free, and real-time detection with high throughput and relatively simple instrumentation. Conceptually, these methods all measure the presence of, or a change in, a biomolecular layer formed on the sensor surface via changes in the interfacial refractive index. Due to a near-linear correspondence between changes in this index and the number of bound molecules, these methods are commonly used to measure the adsorbed molecular mass with high accuracy. Furthermore, by employing intricate modeling and multi-parameter measurements, both the refractive index and thickness of the biomolecular layer can be determined using these methods. Specifically, with state-of-the-art instrumentation and careful calibration of the substrate and solutions, ellipsometry, SMR, and OWLS can be used to quantify dense biomolecular layers with thicknesses down to 2 nm,\textsuperscript{29–32} and using multimode optical excitation concepts, similar deconvolutions are possible in the case of SPR.\textsuperscript{32–34}

In this respect, the dual-mode SPR approach introduced by Rupert et al.\textsuperscript{35} for quantification of nanoparticle size and structure is of particular relevance for our work. They utilized and extended a formalism derived from the characteristic response of an SPR sensor\textsuperscript{35,36} that relates the ratio of the wavelength-shift response of the two considered SPR modes to the size, shape, and RI of the studied systems.\textsuperscript{33} However, due to the large extent of the evanescent field from the surface in SPR (100–400 nm), this method is only fairly accurate in the quantification of the mass of nanoparticles on this or smaller length scale (e.g., tens of nanometers), and thus it is, among others, not capable of characterizing the (change of) shape of nanoparticles with sizes smaller than few tens of nanometers.

In contrast, localized surface plasmon resonance (LSPR) based sensors hold promise for the characterization of analytes of few tens of nanometers and smaller due to the significantly shorter field decay lengths\textsuperscript{35} and have been successfully employed to determine distances of few nanometers, e.g., among two plasmonic antennas and a mirror between and an antenna and a biological layer.\textsuperscript{36–39} Furthermore, they have been used to scrutinize changes in the shape of adsorbed biomolecules\textsuperscript{40–42} and biological nanoparticles, such as lipid vesicles under various conditions.\textsuperscript{43–47} and have been employed to investigate the remodeling of a supported lipid bilayer with the formation of buds and tubules.\textsuperscript{48} In such studies, the LSPR sensors can be viewed as a nanoplasmonic ruler that enables thickness measurements. To this end, in a very recent attempt to combine SPR and LSPR, Mataji-Kojouri et al. have developed a Fabry–Perot cavity array that supports these modes in the same structure. Although this solution performs better than SPR nanorulers in that it is able to determine the thickness of a biomolecular layer in the range of 10–100 nm, the obtained resolution is limited to 4 nm.\textsuperscript{31}

To push the plasmonic nanoruler concept to the regime where an accurate layer thickness determination becomes possible with sub-nanometer resolution, we introduce here a dual-band nanoplasmonic ruler comprising two mixed populations of plasmonic nanoantennas with distinctly different sizes that gives rise to two independent LSPR peaks in the extinction spectrum. Due to the short-range evanescent fields created by the resonating antennas, this approach enables real-time and accurate thickness and RI determination in the sub 10 nm layer thickness range. To corroborate this dual-band nanoplasmonic ruler concept theoretically, we first thoroughly assess the—a priori not obvious—applicability of the formalism introduced by Rupert et al.\textsuperscript{33} for SPR sensors to LSPR sensors using electrodynamic simulations based on the finite-difference time-domain (FDTD) method and use it to rationally design the LSPR ruler that we subsequently implement in practice. For that purpose, we employ a tailored version of hole-mask colloidal lithography and demonstrate the ability of the nanostructured dual-band nanoplasmonic ruler to accurately measure and temporally resolve the thickness change in different systems and settings: (i) atomic layer deposition of an Al$_2$O$_3$ film in air, (ii) adsorption of 35 nm lipid vesicles with subsequent spontaneous formation of a planar supported lipid bilayer (SLB) on silica in liquid, (iii) adsorption of 7 nm SiO$_2$ nanospheres onto an SLB, and (iv) quantification of the shape changes of adsorbed lipid vesicles during SLB formation, demonstrating sub-nanometer resolution up to a thickness accumulation/change of 60 nm, which constitutes a 1 order of magnitude higher resolution than state-of-the-art SPR nanorulers.

**RESULTS AND DISCUSSION**

**Theoretical Background.** In conventional SPR, the response (or, more specifically, the shift in either wavelength or angle of the SPR minimum) associated with changes in the RI and/or thickness and shape of a nanosized analyte (referred to below as “layer”) in contact with the metal surface of the sensor can be analytically described as (see eq 6 in combination with eq 4 in ref 33)

$$R = S(n_{\text{layer}} - n_{\text{bulk}}) \frac{\nu}{\delta}$$

where $S$ is the sensor sensitivity, $n_{\text{bulk}}$ and $n_{\text{layer}}$ are the bulk and layer RIs, respectively, $\nu$, is the molecular analyte volume per unit area (in fact, this is the average thickness of the analyte layer, i.e., the thickness calculated with the close-packed arrangement of analyte atoms or molecules), $\delta$ is a dimensionless factor taking the decay of the intensity of the evanescent field into account that is defined (eq 7 in ref 33) as a normalized convolution of the analyte-mass distribution with the exponential attenuation function $\exp(-z/\delta)$, and $\delta$ is the corresponding decay length. This expression for $R$ depends on the analyte optical properties via $n_{\text{layer}}$ and geometry via $\phi$, and, accordingly, their values cannot be inferred simultaneously from measurements at a single frequency. With two frequencies (associated below with subscripts 1 and 2), however, this is possible and it is convenient to use the ratio of the two readouts (eq 15 in ref 33)

$$\frac{R_1}{R_2} = \frac{S_1(n_{\text{layer}1} - n_{\text{bulk}})/\phi_1\delta_1}{S_2(n_{\text{layer}2} - n_{\text{bulk}2})/\phi_2\delta_2}$$

In applications, the values of all the parameters (except $\phi_1$ and $\phi_2$) are either known or their ratio can be determined by performing measurements in the thin-layer limit (with $\phi_1 = \phi_2$)
Figure 1. Design consideration for a dual-band nanoplasmonic ruler. (a) FDTD-calculated $\Delta \lambda_{\text{peak}}$ of a Au nanodisk in water covered with thin conformal layers of up to 20 nm thickness and with RI of 1.35–1.5, expressed as eq 8, as a function of the layer thickness (the data points are presented by using BRIS calculated in Figure S1, which is used as a fitting parameter). The dashed lines are the exponential approximation of the LSPR sensitivity, in which the linearity confirms that the SPR model is a good approximation for the inhomogeneous fields in a nanodisk, whose effective decay length, $\delta$, is given by the inverse slope of the dashed lines. The inset shows a to-scale schematic of the simulated system. (b) The effective decay lengths, $\delta$, for nanodisks of 20 nm height and varying diameters in media of different RIs. Error bars represent the confidence intervals of the linear regression in fitting the logarithm of the exponential function in eq 8. The data are offset in the $x$ axis for clarity. (c, d) $\Delta \lambda_{\text{peak}}$ of a nanoplasmonic sensor comprising a Au nanodisk of height 20 nm and (c) 80 nm and (d) 160 nm diameter, coated with a conformal dielectric layer with various thicknesses, $d_{\text{layer}}$ and RIs, $n_{\text{layer}}$ subtracted by $\Delta \lambda_{\text{peak}}$ of the corresponding sensors when $d_{\text{layer}}$ and $n_{\text{layer}}$ are 9 nm and 1.41, respectively. It is clear that, knowing only $\Delta \lambda_{\text{peak}}$, it is impossible to deduce $d_{\text{layer}}$ and $n_{\text{layer}}$, as there are infinite combination possibilities that result in a similar $\Delta \lambda_{\text{peak}}$ compared to when the surface is covered with a layer of 9 nm with an RI of 1.41. (e) Combining the two independent results of (c) and (d) enables an unambiguous determination of both $d_{\text{layer}}$ and $n_{\text{layer}}$, i.e., 9 nm and 1.41, respectively (dashed lines).

$\Delta \lambda_{\text{peak}} = 1, 2$). Then eq 2 can be applied to the layers with an arbitrary fine structure and size, and these properties can be characterized via the ratio $\varphi_1/\varphi_2$. We are interested below primarily in a uniform close-packed layer of thickness $d_{\text{layer}}$ with $n_{\text{layer}} = n_{\text{bulk}}$ (eq 14 in ref 33) and

$$\varphi = \frac{1 - \exp\left(-d_{\text{layer}}/\delta\right)}{d_{\text{layer}}} \frac{\delta}{\varphi_1}$$

(3)

In this case, eqs 1 and 2 can, respectively, be rewritten as

$$R = S(n_{\text{layer}} - n_{\text{bulk}}) \left[1 - \exp\left(-d_{\text{layer}}/\delta\right)\right]$$

(4)

and

$$\frac{R_1}{R_2} = \frac{S(n_{\text{layer1}} - n_{\text{bulk}}) \left[1 - \exp\left(-d_{\text{layer1}}/\delta_1\right)\right]}{S(n_{\text{layer2}} - n_{\text{bulk}}) \left[1 - \exp\left(-d_{\text{layer2}}/\delta_2\right)\right]}$$

(5)

We are now interested to investigate in which way this SPR formalism can be applied to an LSPR sensor. Here we note, that despite the obvious conceptual similarities between SPR- and LSPR-type sensors, it is not $a$ priori clear that the above formalism derived for SPR can be validly extended to LSPR, with the distinctly different decay lengths, $\delta$, for SPR (100–400 nm) and LSPR (few tenths of nanometers) and the markedly different geometrical factors (extended planar vs point/localized-like structure) as the main reasons. Thus, a rigorous analysis using electrodynamic simulations that we do here below is an imperative first step to validate the subsequent development of a dual-band nanoplasmonic ruler. For this purpose, we first recall that, in SPR, the decay of the evanescent field is exponential and the corresponding decay length, $\delta$, is defined by the light frequency and optical constants of the media. In LSPR, in contrast, the evanescent field around sensing nanoantennas contains different terms (dipole, etc.), and the corresponding decay length is roughly proportional to and significantly smaller than the antenna size. In addition, one should operate by the permittivities rather than by RIs. At the simplest level this difference can be taken into account in the dipole approximation by just replacing the exponential attenuation function, $\exp(-z/\delta)$, in the calculation of $\varphi$ by the power-law function, $\sim 1/(R^6 + z)^6$, where $R$ is the length scale (effective radius) characterizing plasmonic nanoantennas. In the context of applications, the difference between these two approaches is often minor. For this reason, we use here the conventional exponential approximation, or more specifically eqs 4 and 5, in the LSPR case in order to articulate the analogy between SPR and LSPR, as has often been done in earlier literature since the first applications of LSPR (see, e.g. ref 49). In particular, we identify $S$ with the bulk refractive index sensitivity, BRIS (to be distinguished from the local sensitivity of an LSPR sensor), and rewrite eq 5 as

$$\frac{\Delta \lambda_{\text{peak1}}}{\Delta \lambda_{\text{peak2}}} = \frac{\text{BRIS}(n_{\text{layer1}} - n_{\text{bulk}}) \left[1 - \exp\left(-d_{\text{layer1}}/\delta_1\right)\right]}{\text{BRIS}(n_{\text{layer2}} - n_{\text{bulk}}) \left[1 - \exp\left(-d_{\text{layer2}}/\delta_2\right)\right]}$$

(6)

where $\Delta \lambda_{\text{peak}}$ ($i = 1, 2$) are the analyte-induced LSPR peak position shifts of two sensing plasmonic nanoantennas. Since both resonances practically measure the same analyte layer in...
the same medium and in our context the dependence of \( n_{\text{layer}} \) and \( n_{\text{bulk}} \) on the light frequency is negligible, i.e., \( n_{\text{layer}} = n_{\text{layer}_1} = n_{\text{layer}_2} \) and \( n_{\text{bulk}} = n_{\text{bulk}_1} = n_{\text{bulk}_2} \), the expression can be further simplified to

\[
\frac{\Delta \lambda_{\text{peak}1}}{\Delta \lambda_{\text{peak}2}} = \frac{\text{BRIS}_1 \{1 - \exp(-d_{\text{layer}}/\delta_1)\}}{\text{BRIS}_2 \{1 - \exp(-d_{\text{layer}}/\delta_2)\}}
\]

Equation 7 forms the basis for our analysis below.

In the LSPR case, as already noted, eqs 6 and 7 correspond to the simplest phenomenological approximation containing one length scale, \( \delta \). This approximation is not exact even in the case of a uniform close-packed layer, because the evanescent field around sensing nanoantennas is inherently not exponential (it depends on their shape and is influenced by the support). Nevertheless, the usefulness of eqs 6 and 7 in the LSPR context has already been illustrated.

To explicitly clarify this aspect in our case, we employ finite-difference time-domain (FDTD) simulations to model LSPR sensors comprising Au nanodisks, with diameters spanning from 60 to 180 nm and thicknesses from 20 to 70 nm. Au (rather than Ag that we later use in our experimentally implemented LSPR nanoruler) is chosen, since it is by far the most commonly used SPR surface (which also was used in ref 33, which forms the basis for our analysis here). The insights obtained from our simulations on Au can be directly translated to other noble metals, such as Ag that we use below, since both metals have a similar plasma frequency of around 9 eV and beyond the interband range (which is the one of interest here, especially due to the red shift caused by the substrate and water) their permittivities are similar.

In our simulations, the Au nanodisks are placed on a substrate with a RI of 1.5 and either they are surrounded by a medium with RIs ranging from 1.33 to 1.5 to emulate a BRIS experiment or they are covered by a thin conformal layer of up to 20 nm thickness with an RI of up to 1.5 to emulate a molecular/thin-layer sensing experiment. For the first scenario, the BRIS is a linear function of the nanodisk dimensions and scales well across the simulated parameter range, as expected (Figure S1). To showcase the key findings for the thin-layer sensing scenario, we use a nanodisk with a diameter of 80 nm and a thickness of 20 nm as an example. However, instead of directly plotting the obtained peak shift \( \Delta \lambda_{\text{peak}} \) vs \( d_{\text{layer}} \) for different RIs of the layer, we modify the former into the form

\[
\log \left[ 1 - \frac{\Delta \lambda_{\text{peak}}}{\text{BRIS}(n_{\text{layer}} - n_{\text{bulk}})} \right] = -\frac{d_{\text{layer}}}{\delta}
\]

which is derived from eq 4 with appropriate parameters for an LSPR sensor (i.e., \( \Delta \lambda_{\text{peak}} \) and BRIS replacing \( R \) and \( S \), respectively). The fit of our FDTD calculations by using the left-hand part of eq 8 is close to linear, as predicted by eq 4 (Figure 1a). Thus, eqs 4 and 7 indeed describe our system in an acceptable way. In addition, our calculations show that, as expected, \( d_{\text{layer}} \) (i) the dependence of \( \delta \) on RIs is very weak and thus can be neglected (Figure 1b) and (ii) \( \delta \) is significantly shorter than the size (diameter) of the sensing nanoantenna and increases with an increase in this size, because the decay of the evanescent field is determined primarily by the shape of the nanoantenna (in the dipole approximation, one has \( \delta \approx R^2 \) / 5).

**Nanoruler Design Considerations.** Having confirmed the overall validity of our formalism for LSPR-based sensing, we apply it to design a dual-band nanoplasmonic sensor surface that we subsequently implement and explore experimentally. In this process, the first design consideration is to choose two plasmonic nanodisk types with spectrally nonoverlapping LSPR modes, different decay lengths, and sufficient sensitivities. To illustrate this concept explicitly, we simulated nanodisks with 80 and 160 nm diameter and identical thicknesses of 20 nm and placed a conformal dielectric thin layer with arbitrarily chosen thickness \( d_{\text{layer}} = 9 \) nm and RI \( n_{\text{layer}} = 1.41 \) on top of them to calculate the induced \( \Delta \lambda_{\text{peak}} \) for both nanodisk sizes for this condition. While this is straightforward, if we subsequently want to reverse this process and back-calculate which combination of \( d_{\text{layer}} \) and \( n_{\text{layer}} \) gave rise to the obtained \( \Delta \lambda_{\text{peak}} \) values for each disk, it turns out to be essentially impossible since, as outlined above, a practically infinite combination of \( d_{\text{layer}} \) and \( n_{\text{layer}} \) will produce a similar \( \Delta \lambda_{\text{peak}} \). To illustrate this condition, we calculated all of these potential matches \( (d_{\text{layer}}, n_{\text{layer}}) \) for both disks independently (Figure 1c,d). Specifically, we plot the values of

\[
\log_{10} \frac{\Delta \lambda_{\text{peak}}}{\text{peak}_{\text{layer}} - \Delta \lambda_{\text{peak}}^{9,141}} = \log_{10} \frac{\Delta \lambda_{\text{peak}}}{\text{peak}_{\text{layer}} - \Delta \lambda_{\text{peak}}^{9,141}}
\]

in that the minima give the combination of \( d_{\text{layer}} \) and \( n_{\text{layer}} \) that results in a peak shift similar to \( \Delta \lambda_{\text{peak}}^{9,141} \). While separately the individual response of each of the two nanodisks is not unique with respect to \( d_{\text{layer}} \) and \( n_{\text{layer}} \), the sum of these two plots yields a single point at which the minima of the two curves intersect, which corresponds to the initially chosen values of \( d_{\text{layer}} = 9 \) nm and \( n_{\text{layer}} = 1.41 \), respectively (Figure 1e). Mathematically, such a distinct intersection point can only be defined if the two disks have distinctly different sensitivities and decay lengths, since the particular dependences otherwise partially overlap rather than intersect each other. This, in turn, would result in a large uncertainty of the unique combination of layer thickness and RI that is compatible with the LSPR response of both disk types. Hence, to realize a dual-band nanoplasmonic ruler, one has to employ two types of plasmonic nanoantennas with not only spectrally well separated peaks but also with distinctly different sensitivities and field decay lengths.

We also note that slight disparities of nanodisk geometry due to process variations during fabrication will not affect the functionality of the sensors, as the two disk geometries are chosen with sufficient differences in their diameters to preserve their unique sensing characteristics even when they are subject to fabrication inaccuracies. At the same time, we note that such variations will result in sensors with slightly different sensitivities and decay lengths and therefore lead to slightly different peak ratio-to-thickness conversion plots for their calibration.

**Nanoruler Fabrication and Characterization.** Conceptually, a nanoplasmonic ruler that can disentangle thickness and refractive index variations as outlined above can be accomplished by executing identical measurements on two separate plasmonic surfaces that feature spectrally separated resonance peaks. However, while such measurements are sufficient if one is interested in steady-state conditions, they cannot temporally resolve the investigated processes and therefore preclude analysis of, e.g., kinetics, since it is almost
impossible to have exactly identical conditions in separate experiments on two different surfaces. Therefore, we develop a nanoplasmonic ruler surface where two nanoantennas of different types with distinctly different sizes and thus plasmon resonance wavelengths are mixed within the same array and thus on the same surface. In this way, only one experiment is required to quantify thickness, refractive index, and adsorbate shape, as well as temporal variations in the properties during dynamic processes.

To implement a dual-band nanoplasmonic ruler in line with this design principle, while simultaneously being compatible with the visible to near-infrared (NIR) wavelength range (400–1100 nm) most commonly used in the field,11 we identify two Ag nanodisk populations with 80 and 210 nm diameter and similar height of 20 nm as the best-suited nanoantennas for our purpose.52,56 Specifically, due to Ag’s narrow LSPR modes and interband absorption threshold of ~325 nm, a distinct spectral separation of the LSPR peaks can be obtained.

To implement these properties on a single surface, we employed a modified version of the hole-mask colloidal lithography (HCL)57 method, using a polystyrene (PS) colloidal suspension for the self-assembly step, in which PS beads of two distinctly different sizes (here 74 and 210 nm nominal diameter) were mixed to create a HCL-mask with uniformly distributed holes of two different diameters defined by the beads (see Methods for details). Using this approach, we were able to produce mixed arrays of two nanodisk types with dissimilar sizes on a substrate in a single HCL fabrication cycle (Figure 2a). Varying the relative concentration of the two types of beads in the mixed suspension offers a means to control the relative abundance of the two nanodisk sizes in the mixed array on the surface and thus the relative intensity of the respective LSPR peak, where the aim was to achieve roughly equal intensities (Figure S2). To this end, mixing 0.02 wt % of 74 nm PS beads and 0.1 wt % of 210 nm PS beads in water results in randomly mixed nanodisk arrays whose extinction spectra exhibit two distinguishable LSPR peaks of similar intensity and with a large spectral separation (Figure 2b–d and also see Figure S3 for the nanodisk size distribution). Finally, to introduce both long-lasting structural integrity and protection from harsh chemical and temperature conditions,52,58–61 as well as to provide a uniform chemical surface, we applied a thin conformal SiO$_3$N$_4$ coating to the sensor surface (Figure 2a). If needed, other coating materials can be utilized (e.g., SiO$_2$, TiO$_2$) to alter the interaction of the adsorbed films/biomolecules with the support.

With the sensor surface at hand, we next experimentally quantify the two key sensitivity descriptors of the two types of nanodisks in the array, namely their BRIS and field decay lengths $\delta$. The BRIS is derived by correlating the shifts of the two LSPR peaks, $\Delta \lambda_{\text{peak}}$, to the RI of the medium the sensor is exposed to (Figure 3a; see Figure S4 for raw data). It is clear that the two nanodisk populations in the mixed array respond independently and exhibit different BRIS, i.e., BRIS$_{\text{small}} = 51$ nm/RIU and BRIS$_{\text{large}} = 184$ nm/RIU. These sensitivities are consistent with previous experimental and theoretical works demonstrating a positive correlation between a plasmonic particle size and BRIS.54,65

To determine the field decay lengths of the two types of nanodisks in the mixed array, we applied the established method of subsequent atomic layer deposition of thin Al$_2$O$_3$ layers and fitting the resulting $\Delta \lambda_{\text{peak}}$ induced by the thickness accumulation of each layer to the local sensitivity of a plasmonic nanoantenna expressed in eq 4.34,52,61,62,66 As depicted in Figure 3b, deposition of conformal Al$_2$O$_3$ thin layers of up to 55 nm gives rise to increasing and eventually saturating $\Delta \lambda_{\text{peak}}$ for both small and large nanodisks. To this end, the small nanodisks reach $\Delta \lambda_{\text{peak}}$ saturation earlier, around a layer thickness of 40 nm, implying insensitivity to thickness change beyond this value. The large nanodisks, on the other hand, still exhibit a discernible $\Delta \lambda_{\text{peak}}$ even beyond a layer thickness of 55 nm due to their anticipated longer field decay length.52,54 To explicitly extract the decay length from our data, we fit the $\Delta \lambda_{\text{peak}}$ response to eq 4 and find $\delta_{\text{small}} = 14$ nm and $\delta_{\text{large}} = 28$ nm. Notably, these values compare well to those of the Au nanodisks simulated above (cf. Figure 1b).

After this analysis we have all the necessary input to construct the nanoruler conversion correlation given by eq 7 for our nanofabricated sensor (Figure 3c). The obtained conversion plot provides a direct translation between the $\Delta \lambda_{\text{peak}}$ ratio between the large and small nanodisks obtained from a measurement and the corresponding thickness of an arbitrary layer deposited on the sensor. This conversion plot is strictly valid only for experiments conducted in an air/gaseous environment. In other words, if the sensor surface is used for a measurement in other media, e.g., water, a new conversion plot needs to be constructed on the basis of sensitivity parameters (in particular the decay lengths) determined in this medium. However, as we explicitly show below, by using a system with well-known thickness and RI in liquid medium, we can simplify
The sensitivity of our nanorulers with others employing LSPR-SPR is on the order of 20 nm. This is obvious when we compare the near-field decay length of the plasmonic nanodisks, which is on the range within which the nanoruler exhibits the highest accuracy compared to other nanorulers. As a key point here, we highlight that the range within which the nanoruler is most suitable for measurements of layers in the few to a few tenths of nanometers thickness range.

Thickness and Refractive Index Determination of Single-Layer Accumulation in Air. With the overall concept and sensor surface established, we now apply it to measure the thickness of a single layer accumulated on the ruler surface. To do this, we can again resort to AlO3 layer deposition, as used above for determining the decay lengths in air (Figure 5a). Starting from the independent Δλpeak determined for both small and large nanodisks upon deposition of subsequent AlO3 layers (cf. Figure 3b), we can construct their Δλpeak ratio (Figure 5b) and, for each of the Δλpeak ratios obtained after addition of a new AlO3 layer, calculate a corresponding AlO3 layer thickness by using the conversion (Figure 5c). Comparing the layer thicknesses obtained in this way by the nanoruler with values obtained by ellipsometry for identical AlO3 layers reveals an excellent agreement for the whole measured range from 2 to 55 nm (Figure 5c). Particularly noteworthy is that the nanoruler is able to distinctly resolve the layer thickness in the sub 10 nm thicknesses regime with a maximum absolute thickness difference between the nanoruler and ellipsometry of only 0.6 nm—a significant improvement in accuracy compared to other nanorulers. Furthermore, as discussed above, the nanoruler is also capable of measuring the RI of the AlO3 layer, which again is in good agreement with the value obtained by ellipsometry (Figure 5d).

Thickness and Refractive Index Determination of Biomolecular and SiO2 Nanosphere Layer Accumulation in Liquid Medium. As a second demonstration of the dual-band LSPR nanoruler, we use it to characterize the multistep deposition of a supported lipid bilayer (SLB), followed by small SiO2 nanosphere adsorption (Figure 6a). Specifically, we first expose the nanoruler sensor to a lipid vesicle suspension (1-palmitoyl-2-oleyl-sn-glycero-3-phosphocholine, POPC) in BIS TRIS buffer, while continuously monitoring the RI change per 1 nm change of the layer thickness. The triple sensitivity of the nanoruler, i.e., the change in the absolute Δλpeak ratio per 1 nm change of the layer thickness. The triple sensitivity of the nanoruler, i.e., the change in the absolute Δλpeak ratio per 1 nm change of the layer thickness. The triple sensitivity of the nanoruler, i.e., the change in the absolute Δλpeak ratio per 1 nm change of the layer thickness. The triple sensitivity of the nanoruler, i.e., the change in the absolute Δλpeak ratio per 1 nm change of the layer thickness.
tracking the $\Delta \lambda_{\text{peak}}$ of the two disk populations. Once saturation of the $\Delta \lambda_{\text{peak}}$ is reached, which together with the observed characteristic “kink” in the plasmonic sensor signal (at ca. minute 10) imply that the POPC vesicles have ruptured and formed an SLB on the nanoruler, a rinsing step with pure buffer is applied to remove excess vesicles. Subsequently, we expose the nanoruler to a suspension of 7 nm SiO$_2$ nanospheres, which physisorb onto the SLB. At the end, once $\Delta \lambda_{\text{peak}}$ saturation has again been reached, a pure buffer rinse is applied to remove unbound spheres, leaving a monolayer of SiO$_2$ nanospheres on the SLB. It is noteworthy that, in these experiments, the SLB represents a nearly perfectly uniform layer and accordingly can be characterized by using the nanoruler under consideration. In contrast, SiO$_2$...
nanospheres represent a heterogeneous layer, and it is expected to be characterized by the nanoruler with the simplest expression (eqs 6 and 7) only provided the nanosphere size is smaller than or comparable to $\delta$ that corresponds to the smaller sensing nanodisks. The size of the SiO$_2$ nanospheres chosen for our experiment satisfies this condition.

To start the quantitative analysis and discussion of this experiment, we plot the $\Delta \lambda_{\text{peaks}}$ signals of the small and large nanodisks as a function of time, along with the specific steps described above (Figure 6b). Comparing the $\Delta \lambda_{\text{peaks}}$ signals after the first rinse with the starting point of the experiment reveals an irreversible $\Delta \lambda_{\text{peak}}$ of 2.2 nm for the small-disk peak and of 4.3 nm for the large-disk peak, in good agreement with results from plasmonic sensors with single-type nanodisks, thereby confirming the SLB formation. Looking then at the SiO$_2$ nanosphere adsorption phase, a sudden $\Delta \lambda_{\text{peak}}$ and distinct increase and saturation of $\Delta \lambda_{\text{peak}}$ for both nanodisk sizes occur, corroborating the adsorption of nanospheres on the SLB. At this point, we also note that we observe different trends during the rinsing step following the exposure to POPC vesicles and SiO$_2$ nanospheres in that in the former case both $\Delta \lambda_{\text{peak}}$ signals decrease, while they increase in the latter case. Intuitively, one could assign such a peak change to a decrease and increase of the layer thickness, respectively, which, however, may not be the case, as we discuss below.

As the next step, we plot the $\Delta \lambda_{\text{peaks}}$ ratios for the entire POPC and SiO$_2$ nanosphere deposition, which reproduces the key features corresponding to the different steps of the process (Figure 6c). In particular, we highlight the distinct break in overall trend at the position of the “kink”, where vesicle rupture is initiated. Next, to now be able to derive the ratio-to-thickness conversion plot, the field decay lengths of the small and large nanodisks in water are required. To obtain them, we can utilize the formed SLB, since its thickness and RI are well-known and have been quantified in multiple works to be $\sim$5 nm and $\sim$1.48, respectively. Here it is important to note that the formed SLB is assumed to be a nearly perfect uniform layer. While this holds for SLBs formed using POPC lipid vesicles on oxidized Si$_3$N$_4$, the SLB should be independently characterized in case the lipid composition, vesicle size, surface chemistry, and cleaning protocol of the substrate is changed. To this end, high-quality SLB formed on a nanodisk array similar to our case here has been confirmed. Now referring to the conversion plot, by using the thickness and RI of SLB, we can back-calculate the decay lengths of the two disks for our system in water through modification of eq 4 to

$$\delta_i = -\log\left(\frac{d_{\text{layer}}}{BRI(\eta_{\text{water}} - \eta_{\text{peak}})}\right)$$

and by assigning the thickness and RI of the SLB to the value of the $\Delta \lambda_{\text{peak}}$ obtained during the SLB formation in our experiment: i.e., 4.3 and 2.2 nm for small and large nanodisks, respectively (Figure 6d). This procedure yields decay lengths of 14 and 29 nm for the small and large nanodisks, respectively, which are slightly different from those in air derived above, as expected. With this input, we construct the conversion plot for a water environment (Figure S6). This method of determining the decay length by using a well-known system such as an SLB is (much) less tedious than using subsequent deposition of Al$_2$O$_3$ layers, as we have done first. Furthermore, and most importantly, it has the additional advantage that an SLB can be efficiently removed by mild detergents after such a calibration experiment, making the nanoruler available for subsequent experiments on a system with an unknown thickness and/or RI (Figure S5).

As the final step, we use the conversion plot to extract the thickness evolution of the layers on the surface of the nanoruler during the course of our experiment (Figure 6d). Focusing again first on the SLB formation phase, we find that at the end of the rinsing step the SLB exhibits a thickness of 5 nm, which is 1 nm less than that prior to rinsing but after completed SLB formation. This can be attributed to the removal of excess lipids and lipid vesicles associated with the SLB during the rinsing and gives a first indication of the detection limit of our nanoruler. At the same time, we also highlight that the 5 nm thickness value per se is neither surprising nor an indication of the performance of the nanoruler, since it was used for the decay length determination above. A much more curious and significant result is observed in the phase before the SLB formation is completed: i.e., during the vesicle adsorption and rupture. Specifically, the data reveal an initial thickness buildup up to around 15 nm, after which a sudden and rapid thickness decrease occurs. Interestingly, the transition point accurately coincides with the “kink” observed in the $\Delta \lambda_{\text{peak}}$ data, which is commonly associated with the onset of vesicle ruptures when they have reached their critical surface concentration (cf. Figure 6b). Hence, this experiment confirms the mechanism proposed to be responsible for the “kink” in a plasmonic sensor signal. Furthermore, as we elaborate later below, by establishing a correlation between the $\Delta \lambda_{\text{peak}}$ ratio of our nanoruler and the geometry of adsorbed vesicles, we can quantitatively measure the degree of deformation of vesicles at the critical coverage before rupture.

Focusing here first on the SiO$_2$ nanosphere adsorption, we see a distinct thickness increase from 5 to 16 nm, followed by a slightly reduced thickness of 14 nm after rinsing, which we attribute to the removal of loosely bound nanospheres. Since this is a cumulative thickness that includes the thickness of the SLB, we can deduce that the formed SiO$_2$ nanosphere monolayer comprises particles with an average diameter of 9 nm. An independent size assessment of the nanospheres using transmission electron microscopy (TEM) reveals an average particle diameter of 11 ± 2 nm, which is in good agreement with the value derived with the nanoruler (inset in Figure 6d). We note that the diameter obtained here is slightly larger than the nominal diameter (i.e., 7 nm) and speculate that this difference arises as a consequence of the method used to
To determine it. To this end, the nominal diameter of the SiO₂ nanoparticles was derived via conversion of the specific surface area (SSA) obtained using the Brunauer–Emmett–Teller (BET) method. ⁷¹ BET, however, only permits characterization of dried samples that are prone to agglomeration and consequently results in a lower apparent SSA and thus a smaller inferred particle diameter. ²

Last, we return to the observation that Δλ<sub>peak</sub> was found to increase during the rinsing after SiO₂ nanosphere adsorption (cf. Figure 6b), which we had tentatively ascribed to a thickness increase of the formed layer. However, as the thickness analysis reveals, this is not the case and we actually observe a slight apparent decrease in the thickness (Figure 6d), accompanied by an increase in the RI of the whole layer (Figure 6e). We speculate that the origin of these observations is the detachment of SiO₂ nanospheres loosely attached to the dense SiO₂ nanosphere monolayer that formed on top of the SLB. This detachment consequently lowers the overall thickness and increases the effective RI of the whole layer. We also note that a redistribution of lipids from the SLB onto SiO₂ nanospheres would have a similar effect on the measured thickness and RI and represents an alternative explanation. Overall, the signal changes during this step are very small, and their full-scale interpretation can thus be generally debated.

To determine the resolution of the nanoruler developed here, we assess its noise in terms of both the Δλ<sub>peak</sub> ratio and the deduced layer thickness at two different cases. Figure 6f,g shows the acquired Δλ<sub>peak</sub> ratios at complete formation of SLB and monolayer of SiO₂ nanospheres, respectively. Clearly, in the two cases the Δλ<sub>peak</sub> ratio noises, σ<sub>λ</sub>, are similar: that is, 0.004. This number is extremely low, and referring back to Figure 4, it is lower than the nanoruler sensitivity and therefore, considering a detection limit of 3σ, it confirms the nanorulers’ ability to resolve sub 1 nm thickness changes up to an accumulated thickness of 60 nm. Indeed, this claim holds true also when we infer the resulting thickness determination noise, σ<sub>h</sub>, on the scale of 0.13 nm (Figure 6h,i). Therefore, with the limit of detection defined as 3σ<sub>h</sub> on our nanoruler should in principle be able to distinguish thickness differences of ~0.5 nm for layers in the few tens of nanometers thickness range. This is among the highest resolutions achieved for a functional optical nanoruler. ²²,³¹

Determination of the Degree of Vesicle Deformation prior to Rupture. As the last analysis related to the capability of our nanoruler, we investigated the dynamic changes of the response upon SLB formation in an attempt to determine the thus far elusive degree of deformation of adsorbed vesicles at the onset of SLB formation. As illustrated in Figure 6a, upon adsorption, vesicles are expected to conform to squished, truncated spheres, whose deformation at a critical elongated contact to the support triggers rupture and fusion with nearby vesicles and thus defines the onset of SLB formation. Identifying the vesicle deformation required for this onset of rupture and fusion at the critical vesicle coverage constitutes one of the most central and longstanding questions in this field. ⁴⁴,⁴⁷,⁷³–⁷⁵ To this end, the related indirect data have long been indicative that the deformation required is sizable but not dramatic (see e.g. ref ⁷⁶).

To set the stage for such determination using our nanoruler, it is crucial to recall that eq 4 operates at the level of a uniform film. In the case of adsorbed deformed vesicles, however, the observed signal should be represented as a sum of two signals corresponding to two effective films or, more specifically, to a planar region with a thickness equal to that of the SLB with a contact length defined by radius a and to a truncated spherical shell with the SLB thickness, radius, and height dependent on the extent of deformation (Figure 7a). In other words, eq 4 is obviously insufficient or not fully sufficient for such a case. However, as already noted, eq 4 can be extended as previously proposed for dual-band SPR ⁴⁴,⁴⁷,⁷³ or single-band LSPR. ⁴⁴,⁴⁷,⁷³ Following this line, we illustrate how the former formalism can be applied to our dual-band LSPR ruler.

To give an accurate contribution of the deformed vesicle shape to the optical signal in our sensor, we replace eq 3 by eq S1 in ref ³³ (note that there is a misprint that we correct here)

\[ \varphi = \frac{a^2 + 2\rho \delta}{1 - \exp\left(-\frac{\rho + \sqrt{\rho^2 - a^2}}{\delta}\right)} \] ¹¹

where \( \rho \) is geometrically connected to a through

\[ \rho = \frac{(4r - a^2/r)}{\sqrt{16 - 8a^2/r^2}} \] ¹²

Figure 7. Quantifying the deformation degree of vesicles prior to rupture and SLB formation. (a) Definition of the parameters used to quantify the deformation of an adsorbed vesicle which is represented by a truncated sphere with the assumption that its surface area is preserved. \( r \) is the radius of an intact vesicle, \( h \) is the vesicle height, \( \rho \) is the radius of a deformed vesicle, and \( a \) is the radius of the vesicle—support contact region. (b) Nanoruler conversion plot which translates the Δλ<sub>peak</sub> ratio of the large and small nanodisks (according to eq 13) into the contact length 2a of the deformed vesicles on top of the sensor. Translating the Δλ<sub>peak</sub> ratio at the onset of rupture (i.e., Δλ<sub>peak</sub> ratio of 2.18; cf. Figure 6c) to 2a results in a critical contact length of 35.4 nm (dashed line), which is comparable to the initial vesicle diameter. (c) To-scale schematic of the adsorption and rupture processes of the studied vesicle. The vesicle adsorbs on the support and relaxes until the contact length becomes close to its initial diameter and rupture is initiated, provided the vesicle coverage becomes equal to or is slightly above the critical coverage.

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with \( r \) being the initial radius of the vesicles (Figure 7a). Using eqs 1 and 11, and again converting the relevant parameters to the corresponding LSPR analogues, we express the \( \Delta \lambda_{\text{peak}} \) ratio of our nanoruler to the deformation degree of vesicles expressed via the contact length (Figure 7b)

\[
\frac{\Delta \lambda_{\text{peak}1}}{\Delta \lambda_{\text{peak}2}} = \frac{\text{BRIS}_{\text{large}} \left( \frac{a^2}{\delta_{\text{rep}}} + 2\rho \left( 1 - \frac{\rho}{\rho + \sqrt{\rho^2 - x^2}} \right) \right)}{\text{BRIS}_{\text{small}} \left( \frac{a^2}{\delta_{\text{rel}}} + 2\rho \left( 1 - \frac{\rho}{\rho + \sqrt{\rho^2 - x^2}} \right) \right)}
\]

(13)

To finally identify the critical contact length of the deformed vesicles prior to rupture, we go back to the data presented in Figure 6c. As previously discussed, the onset of the vesicle rupture is marked by the sudden drop in the \( \Delta \lambda_{\text{peak}} \) ratio, where the ratio reaches a value of 2.18. By using the conversion plot presented in Figure 7b, the critical contact length is found to be 35.4 nm (with a corresponding height of 24.4 nm). This result is compelling, as it suggests, that the vesicles will only rupture once their contact length to the support is as wide as its original diameter (Figure 7c). In a more general context, our quantitative result is comparable with those suggested for larger vesicles (~100 nm) on TiO\(_2\) by using LSPR, and for vesicles (~170 and ~100 nm) linked to the support via biotin–streptavidin complexes studied by using SPR and LSPR, respectively.

**CONCLUSIONS**

In summary, we have developed a dual-band nanoplasmonic ruler, capable of determining in real time the change in thickness and refractive index of arbitrary (multi)layers and the shape of nanoparticles deposited on top of it, with sub-nanometer resolution. We achieved such a functionality by theoretically and experimentally devising a plasmonic sensor that exploits the conversion between LSPR and the corresponding LSPR analogues, we express the \( \Delta \lambda_{\text{peak}} \) ratio of our nanoruler to the deformation degree of vesicles expressed via the contact length (Figure 7b)

**METHODS**

**Sensor Fabrication.** Hole-mask colloidal lithography (HCL) was used to fabricate the sensors. The details of the process undertaken (e.g., materials, fabrication steps and equipment) are described elsewhere. Specific to the current work, a mixture of polystyrene beads with nominal diameters of 74 and 210 nm (Interfacial Dynamics Corporation) was diluted in Milli-Q water. To ensure thorough mixing, the suspension was sonicated for at least 30 min. Specific to the HCL process, the tape-stripping step was done twice to ensure all (differently sized) polystyrene beads were completely removed. As a final step, the thin conformal Si\(_3\)N\(_4\) coating layer was deposited in an STS PE-CVD system.

**Chemicals and Materials.** Anhydrous chloroform (C 99%), glycerol (C 99%), HCl (1 M), NaCl (C 99%), bis(2-hydroxyethyl)-aminotris(hydroxymethyl)methane (Bis-Tris, C 98%), and 1-palmitoyl-2-oleoyl-glycero-3-phosphocholine (POPC) were purchased from Merck Sigma-Aldrich (Darmstadt, Germany). The water used was of Milli-Q purity (resistivity 18.2 \( \Omega \) cm, Merck Millipore, Molsheim, France). All buffers had pH = 7.0, 150 mM NaCl, and 10 mM Bis-Tris. The pH was determined using a Mettler Toledo (Ohio, US) pH meter. Buffers were sterilized either by autoclaving at 120 °C for 20 min or by sterile filtration using 0.22 \( \mu \)m Stericup-GV Sterile Vacuum filters (Millipore, France). The colloidal amorphous Si\(_2\)O\(_4\) nanospheres (Bindizil 30/360; the first number denotes the weight concentration, wt %, and second number the average surface area per particle, \( m^2/g \)) were obtained from Akzo Nobel PPC AB (Gothenburg, Sweden). The nominal diameter (7 nm) was calculated as the equivalent spherical diameter based on SSA measurements.

**POPC Vesicle Preparation.** POPC was dissolved in chloroform and dried in a 50 mL round flask under vacuum at 60 °C using a rotavap setup. The dried lipids were left under vacuum overnight to get rid of any residual chloroform. The dried POPC was then rehydrated in H\(_2\)O-based buffer to a concentration of 1 mg mL\(^{-1}\), followed by a very brief bath sonication to dissolve any small traces of lipids on the walls of the flask. The POPC solution underwent five freeze/thawing cycles. After which, the solution was tip-sonicated for 30 min with intervals of 2 s pulse followed by 3 s pause to avoid overheating of the sample. Afterward the sample was centrifuged at 20000g for 30 min to get rid of any residuals from the tip of the sonicator. The POPC solution was finally extruded 11 times through 30 nm polycarbonate membranes (Whatman, UK) using a mini-extruder (Avanti, USA). The resulting vesicles are typical 35 nm in diameter, as determined using dynamic light scattering (DLS).

**Flow Measurements.** A commercial titanium flow cell (XNano, Insplorion AB) was used. All flow experiments were conducted under a constant flow of 100 \( \mu \)L/min, as regulated by a peristaltic pump (Ismatec). The sensor was illuminated using a fiber-coupled halogen lamp (AnaLight-Hal, Avantes), while the extinction spectra were continuously recorded by a fiber-coupled fixed grating spectrometer (AnaSpec-HS-TEC, Avantes). Bulk refractive index sensitivity was derived by exposing the nanoruler surface to mixtures of Milli-Q water (Millipore) and ethylene glycol (Sigma-Aldrich) at the mixing ratios 100:0, 80:20, 60:40, 40:60, and 20:80 wt %. The \( \Delta \lambda_{\text{peak}} \) response was derived by fitting a Lorentzian to the spectra. Prior to flow experiments, the sensor was exposed to UV/ozone for 3 min. This UV/ozone treatment transformed the N\(_3\)-coating surface to Si\(_2\)O\(_4\) with the Si\(_2\)O\(_4\) thickness depending on the O\(_2\) partial pressure, UV irradiance, and duration of exposure of the surface.

**Decay Length Determination Using Al\(_2\)O\(_3\) Layer-by-Layer Deposition.** To determine the decay lengths of the two nanodisk populations on the nanoruler surface, subsequent thin Al\(_2\)O\(_3\) layers were grown by atomic layer deposition (ALD, Oxford FlexAl). Intermittently, the layer thickness (deposited on an analogous silicon chip simultaneously) was evaluated by ellipsometry (J.A. Woollam M2000) and the extinction spectra were recorded using a Cary 5000 spectrophotometer. Great care was taken to ensure that the spectra were always acquired from the same spot on the sample.

**TEM Measurements.** To enable imaging by TEM, the colloidal silica particles were deposited on commercial electron-transparent substrates consisting of a holey-carbon film on a copper grid. The particles were imaged using a FEI Tecnai T20 microscope, equipped with a LaB\(_6\) filament and operated at 200 kV.

**FDTD Simulations.** The electromagnetic simulations were carried out using the finite-difference time-domain method as implemented in the software FDTD Solutions. The Au nanodisks, whose permittivity was taken from measurements by Johnson and Christy, were
modeled as flat cylinders with both top and bottom edges being rounded. The radius and height of the nanodisks spanned the range from 20 to 90 nm and from 20 to 70 nm, respectively. The nanodisks were placed on a substrate with RI = 1.5. When modeling bulk sensitivity, the superstrate’s RI was varied from 1.33 to 1.5. For local sensing of a conformal layer, the superstrate was taken always as water (n = 1.33). The thickness of the conformal layer, which covered both the nanodisk and the substrate, ranged from 1 to 20 nm and its RI spanned from 1.37 up to 1.5. The simulation volume around the LSPR sensor had a mesh step of 0.5 nm. Perfectly matched layer (PML) absorbing boundary conditions were used to terminate the simulation spanned from 1.37 up to 1.5. The total-field/scattered-field scheme was introduced via a total-field/scattered-field scheme.

ASSOCIATED CONTENT

Data Availability Statement
A preprint version of this work is published elsewhere.82

Supporting Information
The Supporting Information is available free of charge at https://pubs.acs.org/doi/10.1021/acsnano.2c04948.

Bulk refractive index sensitivity—geometry correlation in Au nanodisks, physical and sensitivity characterizations of the dual-peak nanorulers, and construction of Δλpeak ratio—layer thickness in a single experiment in liquid medium (PDF)

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F.A.A.N., V.P.Z., F.H., T.J.A., and C.L. conceived the idea. F.A.A.N. fabricated, characterized, and performed measurements on the nanorulers, analyzed the data, and wrote the manuscript. D.S. and T.J.A. executed the FDTD simulation. A.A. and F.H. suggested and prepared the vesicles and buffer solution. P.O. and I.D. participated in fabrication and measurements of the nanorulers. S.N. carried out the TEM measurements. V.P.Z. and F.H. provided the analytical expression for the approach. C.L. coordinated the project. All authors critically commented on and revised the manuscript.

Notes
The authors declare the following competing financial interest(s): C.L. is a cofounder of a company that markets nanoplasmonic sensors. The rest of the authors declare no competing interest.

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