Identifying Eigen-like hydrated protons at negatively charged interfaces

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Despite the importance of the hydrogen ion in a wide range of biological, chemical, and physical processes, its molecular structure in solution remains lively debated. Progress has been primarily hampered by the extreme diffuse nature of the vibrational signatures of hydrated protons in bulk solution. Using the inherently surface-specific vibrational sum frequency spectroscopy technique, we show that at selected negatively charged interfaces, a resolved spectral feature directly linked to the H\(_3\)O\(^+\) core in an Eigen-like species can be readily identified in a biologically compatible pH range. Centered at \(\sim2540\) cm\(^{-1}\), the band is seen to shift to \(\sim1875\) cm\(^{-1}\) when forming D\(_3\)O\(^+\) upon isotopic substitution. The results offer the possibility of tracking and understanding from a molecular perspective the behavior of hydrated protons at charged interfaces.
The hydrated proton (H\(^+\)) in concert with the OH\(^-\), is arguably the most important ion in aqueous solution, playing a prominent role, if not, vital role in a variety of biological, chemical, and geological processes. It represents the essence of a concept as widely used and popularized as pH, and is obviously fundamentally involved in all acid/base chemistry. Despite recent experimental\(^{3-7}\) and theoretical advances\(^{4,8-10}\), a comprehensive molecular understanding of hydrated protons in solution remains elusive. Vibrational spectroscopy, being sensitive to hydrogen bond strength and dynamics, has been the method of choice for determining the molecular structure of the hydrated proton\(^{10}\). However, concentrated acid solutions give rise to extremely diffuse vibrational signatures that extend over at least 2000 cm\(^{-1}\)\(^{1,4,10}\), a fact that reflects the wide-ranging molecular distortions expected in the structural motifs, but at the same time makes the bands challenging to assign to specific species or conformers. In this sense, the structure of the hydrated proton in terms of Eigen\(^{11}\) (H\(_2\)O\(_4\)\(^{+}\)), Zundel\(^{12,13}\) (H\(_2\)O\(_2\)\(^{+}\)) or more delocalized motifs continues to be lively debated\(^{10}\). An important improvement in our understanding came from gas-phase studies of clusters of hydrated protons H\(^+\)(H\(_2\)O)\(_n\), cryogenically cooled to 20 K\(^{1,2,14}\). The clusters limit the motifs accessible to the proton, generating well-resolved IR spectral features that have been directly linked to Zundel and Eigen structures, and are also used as a benchmark for testing the accuracy of different computational methods\(^{8,10,15}\). Though useful, the results from low-temperature gas-phase clusters are not necessarily transposable to condensed phases at ambient conditions\(^{6,16}\). At room temperature, we require background subtraction and the deconvolution of vibrational spectral features to obtain indirect information of the structural motifs\(^{15,16}\). A precious insight has been provided by ultrafast two-dimensional infrared (2D-IR) spectroscopy, where by connecting the coupled resonances at different frequencies, distinct species have been identified in solution\(^{6,7}\). The current consensus leans towards the proton in the bulk liquid being primarily hydrated by two flanking water molecules in a Zundel-like configuration\(^{4,7}\).

The scenario can be different at surfaces. The orientational constraints and asymmetric environment imposed by the interface may reduce the number of structural possibilities, and consequently, result in more resolved features. Vibrational sum frequency spectroscopy (VSFS), a second-order non-linear optical technique with an intrinsic surface specificity, offers the opportunity to yield vibrational spectra from molecules at interfaces\(^{17}\). Under the electric-dipole approximation, VSFS only detects molecules with a net polar orientation, which are typically found in the noncentrosymmetric environment of an interface\(^{18}\). The air/liquid surface of concentrated acid solutions has been the subject of several VSFS studies\(^{19-23}\), but they have primarily focused on the OH stretching region of interfacial water molecules (>3000 cm\(^{-1}\)). Although some of the spectral changes observed, particularly at ~3200 cm\(^{-1}\), were linked to the hydrated proton\(^{21}\), other interpretations associate them instead to an increased number of probed water molecules in the diffuse double layer, which extends upon charging of the surface\(^{22,24}\). With the exception of a couple of studies on neat acid solutions\(^{20,25}\), where no resolved resonant features were detected, the proton continuum region (<3000 cm\(^{-1}\)) on surfaces has largely been neglected.

Here, we use VSFS to probe the proton continuum spectral region of negatively charged liquid/vapor interfaces and identify resolved features associated with hydrated protons having a preferred orientation. The charged surfaces consist of Langmuir monolayers exposing either carboxylic acid or sulfate groups to solution. The associated negative surface potential results in surface hydronium ion concentrations that are orders of magnitude higher than in the bulk, making the spectral features detectable at ambient pH. From the analysis of the VSFS spectra at different polarization combinations and comparison with gas-phase cluster, 2D-IR, and Raman/IR MCR studies, we assign the band observed at ~2540 cm\(^{-1}\) to the antisymmetric stretch of an Eigen-like species.

**Results**

**Carboxylic acid Langmuir monolayers.** The starting point is the conventional homodyne SF spectra at the liquid/vapor interface of an arachidic acid Langmuir monolayer on a sodium chloride aqueous subphase at ambient pH (Fig. 1). The twenty carbon long fatty acid forms an insoluble monolayer that exposes the carboxylic acid headgroups to solution, and the hydrophobic alkyl chains towards the gas phase. The packing density can be varied by moving the barriers of the Langmuir trough. The spectra presented have been collected at a constant surface pressure of 20 mN m\(^{-1}\), where the monolayer is found well-packed in a tilted condensed phase with an average area per molecule of 20 Å\(^2\), as can be deduced from the surface pressure vs. molecular area isotherm (see Supplementary Note 1 and Supplementary Fig. 1). Although the intrinsic pK\(_a\) of these fatty acids is similar to that of shorter chain carboxylic acids (i.e., pK\(_a\) ~5), at the surface, when only the pH determining ions are present in solution, the apparent pK\(_a\) is ~10.8\(^{26}\). The negative charge and accompanying surface potential result in surface proton concentrations that are several orders of magnitude higher than in the bulk. Moreover, the charging behavior upon addition of monovalent ion salts to solution has been shown to be consistent with the Gouy–Chapman theory for concentrations ≤50 mM\(^{26,27}\).

Several molecular structural details of the interfacial region can be extracted from the spectra collected at the two different polarization combinations (i.e., SPS and SSP) shown in Fig. 1. The sharp peaks found between 2050 cm\(^{-1}\) and 2250 cm\(^{-1}\) are all linked to the alkyl chain of the fatty acid, and are primarily stretching modes of the terminal methyl group\(^{26}\). The absence of features from CD\(_2\) groups, indicate that the monolayer is conformationally well-ordered in an all-trans configuration\(^{28}\), consistent with the high packing densities of the tilted condensed phase. At lower frequencies, the peak at ~1720 cm\(^{-1}\) observed in both polarization combinations, is assigned to the C=O stretch of the uncharged form of the carboxylic acid headgroup\(^{26,29}\). The spectra show no features linked to the charged carboxylate moieties, which are expected at ~1408 cm\(^{-1}\) and ~1535 cm\(^{-1}\)\(^{26}\). At pH ~6 and a NaCl concentration of 1 M, the carboxylic acid modes are below the detection limit, yet the monolayer is expected to be ~0.5% deprotonated, as estimated from the Gouy–Chapman model\(^{26}\). Nevertheless, despite the relatively small surface charge (i.e., ~4 mC m\(^{-2}\)), the low ionic strength of the subphase ensure a substantial surface potential that is in the order of ~200 mV\(^{35}\). At higher frequencies, between 3100 cm\(^{-1}\) and 3650 cm\(^{-1}\), the OH stretching bands from water in the interfacial region are apparent (the OH stretch from the hydrogen bonded carboxylic acid gives rise to a weak broad band centered at ~2900–2950 cm\(^{-1}\)\(^{30}\). The signal primarily originates from water molecules directly interacting with the carboxylic acid headgroup\(^{26,31}\), with only a small contribution, if any, from water molecules in the diffuse double layer. At 1 μM the Debye length (i.e., ~300 nm) is significantly longer than the non-linear coherence length of the experimental geometry (Δk\(_z\) ~50 nm), and most of the signal generated within the diffuse double layer cancels due to destructive interference\(^{32,33}\).

Spectral features of hydrated protons at charged interfaces. Central to this study is the band observed at ~2540 cm\(^{-1}\) in the SPS spectrum (Fig. 1b), which is located far from any vibrational
mode expected from the fatty acid or aqueous subphase, but within the proton continuum range of concentrated acid solutions. To confirm that the observed vibrational mode involves the displacement of an OH bond, isotopic substitution experiments were performed using D₂O. The two times heavier deuterium atoms cause the vibrational frequencies to shift within the harmonic level towards lower energies by a factor of ~1.36. The SF spectrum of an equivalent fatty acid monolayer on a D₂O solution collected under the SPS polarization combination is shown in Fig. 2. In the spectrum, the broad water band that was in the case of H₂O originally centered at ~3600 cm⁻¹ is seen, as expected, to red-shift to ~2650 cm⁻¹ in D₂O. More interestingly, a peak resolved at ~1875 cm⁻¹ proves that the ~2540 cm⁻¹ band indeed involves an OH stretching vibration. Compared to the OH stretches of water, typically observed between 3000 cm⁻¹ and 3600 cm⁻¹, the significant red-shift of the ~2540 cm⁻¹ band indicates that the OH bonds are more strongly hydrogen-bonded, as is usually the case of water molecules surrounding the proton.

The peak position lies within the range generally assigned to embedded Eigen-like structures (i.e., an H₃O⁺ core, symmetrically solvated by three water molecules). However, this classification is controversial given the extremely diffuse vibrational signature of the hydrated proton in bulk solution. Although the cryogenically cooled cluster behavior cannot be readily extrapolated to the bulk liquid at room temperature, their resolved features provide useful insight. The charged delocalized Eigen cation H₃O⁺(H₂O)₃ shows a characteristic peak centered at ~2660 cm⁻¹, unambiguously assigned to the doubly degenerate antisymmetric OH stretch of the Eigen core. This band is also observed in larger gas clusters displaying an Eigen-like motif where the hydronium core is predominantly symmetrically solvated (i.e., H⁺(H₂O)ₙ₋₉₋₁₂), and remains detectable in even bigger clusters (i.e., n = 24), though contributions red-shifted by up to ~600 cm⁻¹ also become apparent in the spectra. In contrast, when the proton is shared by two water molecules in a Zundel-like arrangement (H₂O→H→OH₂)⁺, vibrations involving the core proton in the cluster are further red-shifted by more than 1000 cm⁻¹.

Additional experimental information regarding the assignment and also molecular orientation of the hydrated proton at the surface can be extracted from the SF spectra gathered at different polarization combinations. The hydrated proton feature is strongly observed in the SPS spectrum, but besides a weak non-resonant background it is essentially absent in the PPP polarization combination. This is consistent with the band being assigned to an antisymmetric OH stretch of the C₃v symmetry H₃O⁺ in the Eigen core, with its C₃ axis aligned at, or close to the surface normal, as shown in the theoretical orientational analysis presented in Fig. 3b. The curves depict the expected variations in relative intensities as a function of the tilt angle for the polarization combinations SPS, SSP, and PPP, assuming a delta and a narrow Gaussian distribution of angles (see Supplementary Note 2 for details). However, though the experimental intensity in SSP is significantly weaker than for SPS (Fig. 3a), it is not negligible as predicted by the theoretical
analysis for low tilt angles (Fig. 3b). The discrepancy can be accommodated by considering potential contributions from the symmetric stretch of the C3v Eigen core, which when aligned close to the surface normal, should be preferentially observed in the SSP polarized spectra (see Supplementary Note 2 for details)36,38. Although the symmetric stretch has not been experimentally resolved in any of the previous IR cluster studies, it has been theoretically estimated to lie just ~38 cm$^{-1}$ red-shifted3, overlapping 39, or even blue-shifted 1 relative to the antisymmetric mode, with a cross-section that is almost two orders of magnitude lower than for the degenerate antisymmetric stretch9,40. Given that the SF intensity has a square dependence on the IR and Raman transition moments36,37, the significantly lower IR cross-section will have an obvious effect on the intensity of the symmetric stretching mode. Moreover, even though the mode is expected to be stronger in Raman, due to the non-Condon effect4,41, the contribution of the IR component relative to that of Raman in the SF cross-section, becomes more important at the lower OH stretching frequencies of the Eigen core. Consequently, both elements (i.e., low IR cross-section, and non-Condon effect), indicate that the SF cross-section of the H$_3$O$^+$ symmetric stretch will be significantly lower than for the antisymmetric mode.

**Fatty sulfate monolayers.** To further extend the implications of the results, spectra were also collected at negatively charged surfaces that have as chargeable groups other functionalities than the carboxylic acid moiety. The SPS polarization SF spectrum of a twenty-carbon fatty sulfate Langmuir monolayer is presented in Fig. 4. At the pH and selected surface pressure of the experiment, the fatty sulfate monolayer is found in a liquid expanded phase. With an intrinsically lower pKa the fatty sulfate, even at pH 3.8, is substantially more deprotonated, but also shows a higher affinity for the other monovalent counterions (see Supplementary Note 1 for details). The presence of the hydrated proton peak at ~2540 cm$^{-1}$, proves that it is not unique to surfaces displaying charged carboxylic acid moieties.

**Discussion**

In contrast to bulk studies, the VSF results presented show compelling evidence of a narrow spectral feature linked to a specific hydrated proton configuration. The negative charge and
asymmetric environment imposed by the interface are key elements for this distinction. Under the electric-dipole approximation, VSFS only detects molecules with a net polar orientation that have vibrational modes that are simultaneously Raman and IR active18,36. This typically reduces the number of bands resolved when compared with the linear vibrational spectroscopies. Moreover, the surface electric field associated with the negatively charged interface plays a fundamental role, as it not only causes a substantial increase of the surface concentration of hydrated protons, but also has a direct influence on the adopted configuration and its average net orientation. For instance, the VSFS spectrum of pure water, as well as that of solutions of HCl at pH 2, and HB at pH −0.3, show no resolved resonant features in the proton continuum range20,25, highlighting the importance of having a (partly) charged Langmuir monolayer for detecting the hydrated proton at the surface.

From the observed peak position and polarization dependence, together with the insight provided by the experimental and theoretical studies on small cold clusters, the ~2540 cm$^{-1}$ can be assigned to the degenerate antisymmetric OH stretch of the H$_3$O$^+$ core in an Eigen-like configuration, where the three OH are equivalent (i.e., C$_{3v}$ symmetry). The center position is also in agreement to that proposed from calculated IR and Raman spectra for structures that can be classified as Eigen-like4. The orientational analysis for the antisymmetric stretch presented in Fig. 3b, suggest that the principal axis of the H$_3$O$^+$ core should be oriented close to the surface normal. Although the net polar orientation can not be directly obtained from the homodyne SF spectra presented42, the three hydrogens will most certainly be directed towards the negatively charged interface.

Interestingly, the Eigen-like VSFS signal can be detected in fatty acid monolayers when the bulk hydronium ion concentration is just in the order of a few micromolar or less (i.e., pH ~6). At the negatively charged surface, however, the proton concentration is orders of magnitude higher. At low ionic strengths the charging behavior of the monolayer can be accurately predicted using the Gouy Chapman model26, thus the surface concentration of hydrated protons, but also has a direct influence on the adopted configuration and its average net orientation. For instance, the VSFS spectrum of pure water, as well as that of solutions of HCl at pH 2, and HB at pH −0.3, show no resolved resonant features in the proton continuum range20,25, highlighting the importance of having a (partly) charged Langmuir monolayer for detecting the hydrated proton at the surface.

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The SF signal from the hydrated proton could, in principle, originate from Eigen-like species located in direct proximity to the interface, or further away within the diffuse double layer32,44. However, the fact that the Eigen band is more strongly observed on a 1 μM NaCl subphase than at higher salt concentrations (Fig. 5b), suggests that the origin is from close proximity to the interface. Had the signal been generated from within the diffuse double layer, due to destructive interference, it would have increased with ionic strength in the concentration range considered as experimentally confirmed elsewhere when probing water molecules in the diffuse layer26,45 (i.e., the Debye screening length at 1 μM NaCl is significantly longer than the non-linear coherence length of the SF process32,33). Given that the Eigen-like proton is symmetrically hydrated, one possibility is that the hydrated proton forms a solvent separated ion pair46 with the charged carboxylate and sulfate headgroups. Nonetheless, the hydrated proton must also interact with other competing counterions present at the interface. For the fatty acid monolayers, the proton has a significantly higher affinity than other monovalent cations such as Na$^+$ to interact with the carboxylate headgroup47. This is not the case for the sulfate headgroup48, where the presence of sodium counterions in the subphase could have a detrimental effect on the measured H$_3$O$^+$ core signal.

![Fig. 5 Salt dependence of the hydrated proton spectral feature: theory compared with experiments.](image-url)

**Fig. 5** Salt dependence of the hydrated proton spectral feature: theory compared with experiments. **a** Calculated surface proton concentration as a function of NaCl in the subphase of a fatty acid Langmuir monolayer based on the Gouy Chapman model, for three different pH. **b** VSFS spectra in the SPS polarization of a dAA monolayer on an aqueous subphase with varying concentrations of NaCl at natural pH (surface pressure 20 mN m$^{-1}$, temperature 22 °C). Note that the H$_3$O$^+$ antisymmetric stretch intensity follows the same trend predicted for the surface proton concentration as a function of salt.
In summary, a resolved spectral feature assigned to the anti-
symmetric OH stretch of the H$_2$O$^+$ core in an Eigen-like con-
figuration has been identified at negatively charged interfaces
exposing carboxylic acid and sulfate headgroups to solution. The
fact that Eigen-like protons can be detected in a biologically
relevant pH range, may offer novel perspectives for understan-
ding essential physiological functions involving proton interactions
with cell membrane interfaces. The presence of a band linked to
the charge carrier opens a window of opportunities for potentially
tracking the behavior of hydrated protons in a variety of condi-
tions and systems. Moreover, VSFS could also be used in its phase-
sensitive form and, in time-resolved configurations, to extract
additional information including absolute polar orientation and vibra-
tional dynamics. We anticipate that Eigen-like protons are not
necessarily the only structural motifs with a preferred orien-
tation that can be found at an interface, but at given conditions,
other configurations, in particular, Zundel-like hydrated protons
could well be the preferred species. It is hoped that the informa-
tion provided here may stimulate theoretical and simulation stu-
dies of hydrated protons at charged interfaces.

Methods

Materials and preparation of solutions. NaCl (99.999% trace metal basis, Merck)
was baked at 500 °C for 1 h in order to remove traces of organic contaminants. HCl
36.5% (99.999% trace metal basis, Alfa Aesar), deuterium oxide (D 99.9%, <0.8 μS
– cm$^{-1}$ in conductivity, Cambridge Isotope Laboratories, Inc., MA, USA), chloro-
form (anhydrous grade, stabilized with ethanol, Merck), methanol (99.98%, Merck),
acetic acid (97%, dAA for deuterated arachidic acid, Merck), and sodium eicosyl
sulfate (>95%, Santa Cruz Biotechnology, TX, USA) were used as received. The electrolyte solutions were prepared by serial dilution in either D$_2$O or ultrapure water from an Integral 15 Millipore system (resistivity of
18.2 MΩ cm and TOC < 3 ppb). The solvents used for the fatty acid and fatty
sulfate spreading solutions consisted of pure chloroform, and a mixture of chloroform-methanol in a 1:1 proportion, respectively.

Langmuir trough. The monolayers were formed by spreading a few microliters of
the fatty acid or fatty sulfate solutions on the surface of the subphase placed in a
Langmuir trough (KSV NIMA, Finland, 195 mm length, 50 mm width, and 4 mm
in depth). After a waiting time of at least 10 min to ensure full solvent evaporation,
the monolayers were compressed at a rate of 5 mm per minute. The surface
pressure was measured using a paper Wilhelmy plate. All the VSFS experiments were
carried out using a constant surface pressure and temperature of 22.0 ± 0.5 °C. For the fatty acid case, the surface pressure was 20 mN m$^{-1}$ (~20 Å$^2$ per molecule), while for the fatty sulfate it was set to 2.5 mN m$^{-1}$ (~65 Å$^2$ per molecule). See Supplementary Note 1 for additional details.

VSFS spectrometer. The femtosecond spectrometer has been described in detail
elsewhere, and only a brief description of the key features is given here. The tuneable IR (~100 fs and 1 kHz) and visible pulses (805 nm, tuneable beam shaper,
>20 ps long) are focused at the sample position in a co-propagating geometry at
angles of incidence of 55° and 70°, and pulse energies of ~4 mJ cm$^{-2}$, respectively. The spectrometer features a high degree of automation that allows for simultaneous measurements of the C–D symmetric stretch in the SSP spectra, and can be directly compared.

Surface hydronium concentration from the Gouy–Chapman theory. The proton
concentration at the surface [H$^+$$]_w$ depends on that in the bulk [H$^+$$]_b$, as well as
the surface potential $\psi_0$:

\[
[H^+]'_w = [H^+]_b \exp\left(\frac{-\varepsilon kT}{e} \right)
\]

(1)

where $\varepsilon$, $k$, and $T$ are the elementary charge, the Boltzmann factor, and temperature,
respectively. The surface potential is in turn related to the degree of dissociation $a$
of the carboxylic acid monolayer ($a$), and equilibrium constant $K_a$ for the reaction
HA $\leftrightarrow$ A$^-$$+$$H^+$:

\[
K_a = [A^-][H^+] /[HA_0] = \frac{\alpha}{1 - \alpha} \exp\left(\frac{-\psi_0}{kT}\right)
\]

\[
\psi_0 = \frac{kT}{e} \ln\frac{[H^+]'_w}{[H^+]_w} - \ln K_a - \ln\left(\frac{1 - \alpha}{\alpha}\right)
\]

(2)

The surface potential $\psi_0$ also depends on the concentration of ions in solution
[NaCl], and the surface charge density $\sigma$ (i.e., the degree of deprotonation),
through the Grahame equation:

\[
\sigma = \frac{e}{A_M} = \sqrt{8e_0 kT \sin h\left(\frac{\psi_0}{2kT}\right) \frac{[NaCl]}{\exp\left(\frac{-\psi_0}{kT}\right) \exp\left(\frac{-\psi_0}{kT}\right)}}
\]

(3)

where $e$ and $\varepsilon_0$ are the dielectric constants of water and vacuum, respectively, and $A_M$ is the area per molecule (~20 Å$^2$ per molecule). The surface potential is determined
by simultaneously solving Eq. (2) and Eq. (3) and setting the $pK_a$ to $5.2$.

Data availability

The datasets generated during and/or analyzed during this study are available from the
Corresponding author on reasonable request. The specific data used for plotting the
Figures in the article can also be found in a Supplementary Dataset.

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**Author contributions**

E.T. designed research. E.T, S.S. and A.S. performed research and analyzed data. E.T. wrote the article.

**Competing interests**

The authors declare no competing interests.

**Additional information**

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