Article

Low-Cost Position Sensorless Speed Control of PMSM Drive Using Four-Switch Inverter

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Abstract: A low-cost position sensorless speed control method for permanent magnet synchronous motors (PMSMs) is proposed using a space vector PWM based four-switch three-phase (FSTP) inverter. The stator feedforward $dq$-axes voltages are obtained for the position sensorless PMSM drive. The $q$-axis current controller output with a first order low-pass filter formulates the rotor speed estimation algorithm in a closed-loop fashion similar to PLL (Phase Lock Loop) and the output of the $d$-axis current controller acts as the derivative representation in the stator feedforward voltage equation. The proposed method is quite insensitive to multiple simultaneous parameter variations such as rotor flux linkage and stator resistance due to the dynamic effects of the PI current regulator outputs that are used in the stator feedforward voltages with a proper value of $K$ gain in the $q$-axis stator voltage equation. The feasibility and effectiveness of the proposed position sensorless speed control scheme for the PMSM drive using an FSTP inverter are verified by simulation and experimental studies.

Keywords: permanent magnet synchronous motor (PMSM); space-vector PWM (SVPWM); four-switch three-phase (FSTP) inverter; reduced switch inverter; component minimized inverter; position sensorless control; stator feedforward voltage control (FFVC)

1. Introduction

Permanent magnet synchronous motors (PMSMs) with sinusoidal shape back-electromotive force (EMF) require precise position sensors such as an optical encoder and a resolver for field-oriented control (FOC). However, attaching these position sensors to the rotor is associated with cost, space, additional wiring, mechanical burden, weight, noise interference and reliability. Therefore, there is a motivation to eliminate position sensors from the PMSM drive and operate it as “sensorless” or “encoderless”. Although the position sensor is eliminated for sensorless control, the rotor position must be determined only by measured electrical quantities (such as motor currents, inverter direct current (DC)-link voltage, voltages at the motor terminals, etc.). Therefore, current and/or voltage sensors are required to achieve a position sensorless PMSM drive scheme. There are different techniques for sensorless operation of permanent magnet synchronous motors and they are divided into two main groups: (1) model-based methods and (2) saliency and signal injection methods. Sensorless operation of machine model-based methods at zero and low speed is problematic due to motor parameter sensitivity, initial rotor position error, DC drift and flux integration issues, measurement errors of stator current and voltage, inverter and machine nonlinearity. Since model-based methods rely on the amplitude of back-EMF, which is proportional to the rotor speed, these techniques fail in zero and low-speed regions. Therefore, model-based sensorless methods present good results only in the middle and high-speed regions. Saliency and signal injection techniques do not require back-EMF information;
therefore, improved zero and low speed performance along with less parameter dependencies are achieved even under heavy load conditions. However, these sensorless techniques are difficult to implement and produce high audible noise, extra losses, current harmonics, torque ripples, transient disturbances and vibration. The detailed classifications of the sensorless control methods are depicted in Figure 1 [1–7]. Recently, improvements in model-based and signal injection methods for PMSM drives have been investigated in the literature [8–15]. To suppress the unwanted audible noises in the signal injection methods, pseudo-random high-frequency signal injection (HFSI) method is proposed as an alternative to the classical HFSI technique [8,9]. To eliminate the harmonics and improve the estimation of the rotor position in the model-based sensorless control methods, adaptive linear neural (ADALINE) network-based filter is proposed in [10]. In [11], a robust adaptive sliding-mode observer (SMO) with an online inverter nonlinearity compensation method is proposed to reduce the chattering effect of SMO. The proposed method improves the dynamic and steady-state performance of the surface mounted PMSM drive in a low speed region.

Hybrid methods become an alternative approach to improve the issues observed in the model-based sensorless schemes. The combination of sliding mode observer (SMO) and neural networks (NNs) is proposed as an angle compensator to improve the starting and low speed performance of the PMSM drive in [12]. Adaptive synchronous-frequency tracking-mode observer (SFTO) which is a combination of SMO and model reference adaptive system (MRAS) is investigated for a surface mounted PMSM drive in [13]. In [14], a highly accurate rotor position and speed estimation are achieved by eliminating the influence of harmonic components caused by torque fluctuations at high and low speed regions. Two novel nonlinear rotor flux observers, second-order generalized integral flux observer (SOIFO) and second-order SOIFO are proposed instead of a classical pure integrator and Low-Pass Filter (LPF) to eliminate the offset and harmonics in the estimated rotor flux. Therefore, low speed operation of surface mounted PMSM is improved even under resistance variation. In addition, the wide speed range sensorless control can be achieved by combining signal injection methods with machine model-based methods [5]. Hybrid methods are used both with signal injection and model-based methods where seamless transition is performed by switching from a signal injection method to a model-based method above a certain speed threshold. The hybrid seamless control method with a dual-position tracking observer in conjunction with the signal injection and sliding mode observer (SMO) is proposed and evaluated in [15]. However, operation of a wide range of sensorless speed control is achieved, and hybrid sensorless control systems increase the complexity of the overall control system.

In many applications where, especially, low power is demanded such as in consumer products and light electric vehicles, the development of a reduced cost three-phase inverter is essential to decreasing the overall drive cost along with removing the position sensor. The overall price of the three-phase inverter is mainly determined by the number of semiconductor switches. A low-cost inverter topology with a reduced number of switching devices was first presented for an induction machine drive system in [16] as an FSTP inverter in which one of the three-phase windings is connected to the center-tap of the two DC-link capacitors and a comparable performance is achieved to the conventional six-switch three-phase (SSTP) inverter. With this modification, the FSTP voltage source inverter (VSI) topology generates only four non-zero active space vectors without any non-zero vectors in the $a\beta$ plane, as opposed to six active and two zero voltage space vectors in the SSTP VSI counterpart and it is acknowledged as the standard reduced switch inverter topology for three-phase alternative current (AC) drives in the literature.
Figure 1. Classification of the sensorless control methods for a PMSM drive [1–7].

FSTP inverter control topologies have been adapted to both sensored and sensorless PMSM and brushless DC (BLDC) drives in [17–64]. FSTP inverter-based BLDC drive is firstly introduced in [17]. The improvement in speed control performance of [17] is achieved in [18]. In Ref. [19], one of the first attempts of PMSM speed control using an FSTP inverter is performed and compared with an SSTP inverter. In Ref. [20], the BLDC motor with three hall-effect position sensors driven by an FSTP inverter based on a novel current controlled PWM strategy with six commutation modes is proposed. To achieve low-cost sensorless BLDC position control, utilizing crossing detection of the two active phase voltage waveforms with an asymmetric voltage PWM method based on [20] is presented in [21]. In Refs. [22–25], sensorless control methods for a BLDC drive using an FSTP inverter are reported. The position sensorless control of PMSM driven by an FSTP inverter is introduced in [26–28]. In [29], a direct torque control (DTC)-based BLDC motor driven by an FSTP inverter that employed a novel optimum switching table which enables the independent simultaneous control of the electromagnetic torques developed by the phases connected to the inverter legs without requiring explicit stator flux control is achieved. The operation of an FSTP inverter resembles the faulty one-leg of a traditional SSTP inverter. Recent research has focused on the reliability and fault tolerance of an SSTP inverter under faulty one-leg conditions to maintain the stable operation of the overall drive scheme. In Ref. [30], the proper operation of an induction motor driven by an SSTP inverter under a short-circuit fault in one-leg is accomplished without significant disturbance using a proposed fault isolation topology in which the inverter is reconfigured from six switches to only four switches. The faulty condition of an SSTP inverter resembling the operation of an FSTP inverter are investigated for PMSM drives using FOC and DTC schemes in [31–38]. Minimization of torque and current ripples incorporating space vector pulse width modulation (SVPWM) have been investigated for FSTP inverters. In the FSTP inverter, one phase is always attached to the uncontrolled center tap of the two DC-link capacitors; therefore, current waveforms are distorted and unbalanced. Compensation strategies for PMSM and BLDC drives are employed to overcome the current and torque distortion and unbalancing issues of FSTP inverter in [39–45]. Moreover, there have been efforts to reduce the number of current sensors from two to one in FSTP inverter driven PMSM and BLDC drives in [25,46,47]. Intelligent control methods such as fuzzy-logic and ANN type controller strategies have been proposed for FSTP driven
PMSM and BLDC drives in [48–52]. BLDC drives using FSTP inverters with power factor correction (PFC) have been presented in [53,54].

There are several advantages of an FSTP inverter compared to traditional SSTP inverter: although each switch rating in FSTP inverter is higher than the one in the SSTP inverter, the price of total number of switches in FSTP inverter is reduced compared to the one in the SSTP inverter, therefore cost and space are minimized due to the reduction of the number in the semiconductor switches and freewheeling diodes; there are only two driving circuits, therefore complexity of drive and control circuitry are reduced which lowers the overall cost of the drive; due to the elimination of the semiconductor switches, with no change in the amplitude of DC-link voltage, conduction and switching losses are reduced by 1/3; since there is a smaller number of semiconductor switches, the reliability of the converter increases; maximum common mode voltage is only 2/3 of SSTP inverters. Unit cost per kW is targeted to be $13.7 at 2022 R&D targets [65]. Housing and Heatsink costs represent 10% of the total cost. When the cooling system needs to be reduced by 1/3 in the developed system, the heating requirement is around 15% more compared to the six-switch inverter because of the power ratio. In this case, a cost of 1.04 $/kW is achieved. A larger capacitor is required due to the peak in voltage. For this reason, the total cost of the capacitor, which is 14%, is 2.877 $/kW. In signal processing and power solid-state circuitry, a reduction of 1/3 is achieved. The cost is 2.74 $/kW for the signal circuit and 3.1967 $/kW for the power modules. The realized system cost is 12.054 $/kW. Given the 2022 targets, total cost reduction of 12.08% is achieved. Due to the above-mentioned benefits, FSTP inverter topology has been implemented in many low to medium power industrial applications ranging from servo to traction.

However, the FSTP inverter topology has some drawbacks: since one of the motor phase windings has to be connected to the center-tap of the DC-link capacitors, as shown in Figure 2, current flowing from this leg charges one of the capacitors and discharges the other one, therefore it exposes low frequency harmonic contents. This will cause significantly large fluctuations in the DC-link voltage and create considerably large unbalance three-phase currents at the output [55–57]. These unbalanced currents with harmonic components get bigger when the DC-link voltage is lower. Improved controller design is required to balance the capacitor voltages. Moreover, to eliminate the third-order harmonics, a larger value of switching frequency should be selected [58–63]. FSTP inverter control topologies have been adapted to sensorless PMSM drives in [26–28]. In [66], although the sensorless FSTP inverter of PMSM drive is proposed, ANN is used to achieve a sensorless drive which has a complicated algorithm.

The main contribution of this paper is to modify the $dq$-axes stator feedforward voltage control (FFVC) algorithms to achieve a simple, effective and low-cost position sensorless speed control scheme for PMSM drive using FSTP inverters. Normally, the stator feedforward voltages are used to improve the dynamic performance of the FOC of AC drives; however, in this work, they are not only used to improve the dynamic capability of the drive scheme but also are utilized to achieve a simple and effective sensorless control of the FSTP based PMSM drive in which starting under no-load is possible.
without any open-loop start-up procedures. The earlier work that has been developed for induction motors, and permanent magnet synchronous motors which are driven by SSTP inverter in [66–68], respectively are extended for FSTP inverter based sensorless PMSM drives to achieve simple, stable and cost-effective approach under multi-parameter detuning. In [66], flux vector (FV) control is presented for induction motor (IM) as a position sensorless method where the performance is better than V/Hz control but slightly less than indirect field-oriented control (IFOC) [69]. Analysis of the effects of stator resistance variation on the performance of FV and field-oriented (FO) controllers of IM have been proposed in [69] where a back-EMF (back electromagnetic force) detector is developed to reduce the adverse effect of stator resistance on both IFOC, FV and V/Hz control of IM drive with or without position sensors. The performance of the position sensorless FV control of IM in [66] is attempted to be improved in [69] where stator resistance is adjusted based on the error between the reference $d$-axis current and its feedback component. It is indicated in [69] that the proposed method is best suited for low frequency operation.

The remaining part of this paper is organized as follows. The principles of the proposed position sensorless speed control technique is presented in Section 2. In Section 3, experimental results of the proposed FSTP based position sensorless PMSM drive scheme including no-load start-up, steady-state load disturbance, transient speed change under load, and effect of the parameter variations at medium and low speed regions are presented and discussed. Finally, the conclusion is provided in Section 4.

2. Proposed Position Sensorless Speed Control of Four-Switch Three-Phase PMSM Drive Based on Stator Feedforward Voltage Control

2.1. Steady-State and Dynamic Mathematical Models of PMSM

The $dq$-axes dynamic model shown in Figure 3 is used to evaluate the field-oriented control (FOC) of PMSM. The rotating $dq$ frame based stator voltage equations and stator flux flux linkages neglecting the effects of magnetic saturation and magnetic hysteresis are given by

$$v_q = i_q R_s + L_q \frac{d i_d}{dt} + \left( \omega_e L_d i_d + \omega_e \lambda_f \right) = i_q R_s + \omega_e \lambda_q + \frac{d \lambda_d}{dt},$$  \hspace{1cm} (1)

$$v_d = i_d R_s + L_d \frac{d i_d}{dt} - \omega_e L_q i_q = i_d R_s - \omega_e \lambda_q + \frac{d \lambda_d}{dt},$$  \hspace{1cm} (2)

$$\lambda_q = i_q L_q + \lambda_{qr},$$  \hspace{1cm} (3)

$$\lambda_d = i_d L_d + \lambda_{dr},$$  \hspace{1cm} (4)

where $v_d$, $v_q$, $i_d$, $i_q$ are the stator voltages and currents in $dq$ frame, respectively; $R_s$ is the stator resistance; $L_d$ and $L_q$ represent the $dq$-axes inductances; $\omega_e$ denotes the rotor angular electrical speed; $\lambda_d$ and $\lambda_q$ are the $dq$-axes stator flux linkages in which $\lambda_{dr}$ and $\lambda_{qr}$ are the $dq$ frame rotor flux linkages where $\lambda_{dr} = \lambda_f$ is the permanent magnet flux linkage and $\lambda_{qr} = 0$ [70–72]. For surface-mounted permanent magnet synchronous motor, $L_d = L_q = L_s$ where $L_s$ is the stator inductance of the surface-mounted PMSM.

The $dq$-axes steady-state stator voltage equations can be obtained using Equations (1) and (2) considering the derivative terms equal to zero as

$$v_q = i_q R_s + \left( \omega_e L_d i_d + \omega_e \lambda_f \right),$$  \hspace{1cm} (5)

$$v_d = i_d R_s - \omega_e L_q i_q.$$  \hspace{1cm} (6)
2.2. Principles of the Proposed Position Sensorless Scheme

The main purpose of the feedforward voltage control is to transform the dq-axes reference currents into dq-axes reference voltages which are decoupled with each other. The feedforward de-coupling approach computes stator dq-axes voltage references directly by using the steady-state model of the motor given by Equations (5) and (6). As mentioned above, the torque producing component and the flux component are obtained by a q-axis current and a d-axis current reference command signals, respectively. The q-axis current reference component is fed into a first-order time-delay element whose output serves as the input to the de-coupling computing unit. In this way, the torque producing current component response is actually established in advance upon which corresponding stator voltage component \( v^* \), which can ensure that the de-coupling of the motor can be calculated based on the inverse derivation of the motor model. The feedforward de-coupling computing equations are represented by Equations (5) and (6). It is apparent that the feedforward de-couple approach does not only depend on the output of the current regulator to adjust the torque output. Even if the current PI regulators are open-loop, the desired performance of the system can still be achieved, thus ensuring the stability of the system. The d-axis current regulator output can be used to promote the dynamic property while decreasing the impact of parameter variations on the performance of the system. It is seen from Equations (5) and (6) that the currents in the dq-axes can be controlled by the dq-axes voltages and rotor speed \( \omega_e \). In a steady state, rotor frequency is equal to the frequency of the stator voltage. Assuming that the actual currents \( i_d \) and \( i_q \) follow the reference currents \( i^*_d \) and \( i^*_q \) closely in a steady-state, the dq-axes stator feedforward voltage equations for the proposed position sensorless speed control of PMSM driven by FSTP inverter are expressed as

\[
\begin{align*}
    v^*_q &= i^*_q R_s + \left( \omega_e L_d i^*_d + \omega_e \lambda_f \right) + K \Delta v, \\
    v^*_d &= i^*_d R_s - \omega_e L_q i^*_q + \Delta v,
\end{align*}
\]

where \( \Delta v \) is the d-axis current controller output, which is multiplied by K gain and added to the q-axis voltage equation in Equation (7) symbolizing the dynamic term \( L_d i_d / dt \) in Equation (8) to minimize the errors in the PI regulator under dynamic changes in parameters and disturbance and \( \omega_e \) is the q-axis current regulator output. The \( \Delta v \) term in Equation (8) also acts as the dynamic representation in d-axis voltage equation \( L_d i_d / dt \) in Equation (2) to improve the transient response of the sensorless operation. By combining the dynamic stator voltage Equations (1) and (2) and the proposed feedforward stator voltage estimator Equations (7) and (8), K gain is obtained to be proportional to \( L_d \Delta i_q / \Delta i_d \), in which \( \Delta i_q \) and \( \Delta i_d \) are the sample difference of the \( d \)- and \( q \)-axes currents, respectively. Under the dynamic conditions such as load disturbance, reference and parameter changes, a misalignment between the reference frame and the rotor flux vector produces non-zero terms represented by the derivative term in the d-axis voltage which is the output of the d-axis current regulator called \( \Delta v \). Since the feedforward control of \( v^*_d \) is determined by Equation (8) on the assumption of existing field alignment, such a misalignment causing deviation will generate a
correcting signal from the \(i_d\) controller. This signal through a \(K\) gain affects the \(q\)-axis voltage \(v_q^*\) and, therefore, \(i_q\) as well, causing the \(q\)-axis current regulator to accelerate or decelerate the reference frame to reconstruct the correct field orientation and, therefore the accurate rotor speed is obtained. Since the torque increases when the electrical rotor speed increases, as a result the rotor flux linkage angle can be derived from integration of the \(q\)-axis current controller output. Therefore, the estimated electrical rotor speed, related to the torque producing current \(i_q\), is obtained from the output of the \(q\)-axis current regulator through a first order low pass filter. The first order low pass filter at the feedback of the speed estimation loop reduces the transient effects that occur from the output of the \(q\)-axis current regulator. Although the system is equipped with \(d\) and \(q\)-axes current controllers, the internal cross-coupling between the input variables and state variables of the machine is not eliminated under dynamic conditions, therefore the desired decoupled machine structure is not established. The reason is that the electrical rotor position is not determined by the rotor flux linkage vector. It is governed by the \(q\)-axis current error instead, which through the \(q\)-axis current regulator, accelerates or decelerates the reference frame. A nonzero value of the \(q\)-axis rotor flux linkage \(\lambda_q\) indicates a misalignment of the field-oriented reference frame. It is now assumed that the shaft speed \(\omega_r\) changes by a sudden increase of the load torque. The subsequent decrease of rotor speed produces a negative \(d\lambda_q/dt\). Simultaneously, the \(q\)-axis component \(\omega_r \lambda_f\) which is the back-EMF that acts on the stator is increased, therefore the \(q\)-axis stator voltage value increases as well. The consequence is that \(i_q\) rises, delayed by the first order low pass filter time constant, which restores \(d\lambda_q/dt\) to its original zero value after the delay. Before this readjustment takes place, \(\lambda_q\) has already assumed a permanent nonzero value, and field orientation is lost. A similar effect occurs on a change of \(\omega_r\) which instantaneously affects \(d\lambda_q/dt\), while this disturbance is compensated for only after the time delay of the first order low pass filter by the feedforward adjustment of \(v_q^*\) through \(\omega_r\). Undesired perturbations are eliminated by the addition of the first order low-pass filter. Maintaining field orientation still needs further improvement. The signal \(\omega_r \lambda_f\) in Equation (1) contributes to back-EMF which influences the stator current derivative. A misalignment between the reference frame and the rotor flux vector produces a nonzero \(\lambda_q\) value, giving rise to a back-EMF component that changes \(i_d\). Since the feedforward control of \(v_q^*\) is determined by Equation (8) on the assumption of existing field alignment, such a deviation will invoke a correcting signal from the \(i_d\) controller. This signal is used to influence, through a gain constant \(K\), upon the quadrature voltage \(v_q^*\) and hence on \(i_q\) as well, causing the \(i_q\) controller to accelerate or decelerate the reference frame to reestablish accurate field alignment.

At steady-state, the output of the \(d\)-axis current controller \(\Delta v\) and rotor flux linkage \(\lambda_f\) relationships are expressed in per-unit form when \(i_d^* = 0\) using Equation (1) as

\[
\Delta v \propto \frac{\omega_r \lambda_f}{K},
\]

where \(\omega_r\) is constant in a steady-state, hence the rotor flux linkage \(\lambda_f\) is proportional to \(\Delta v\) as

\[
\lambda_f \propto \Delta v.
\]

As opposed to the classical six-switch three-phase (SSTP) inverter, where six non-zero and two-zero voltage vectors exist, only four active non-zero voltage space vectors and no zero voltage vectors are available in FSTP inverters, as shown in Figure 4 where phase-a is connected to the centre-tap, as illustrated in Figure 2. Compared to the six-switch counterpart, since each vector is aligned to an axis, vector representations are simple in FSTP inverter topology enabling more easier space vector pulse width modulation (SVPWM) strategy. Maximum line to neutral voltage is \(V_{dc}/(2\sqrt{3})\) and can be used to normalize the space vectors \(V_1 = V_3 = V_{dc}/\sqrt{3}\) and \(V_2 = V_4 = V_{dc}/3\). In the structure of the SVPWM switching method for the proposed FSTP inverter based sensorless scheme, the reference voltage vector in each sector can be represented with the two closest voltage space vectors and zero voltage vectors in \(a\beta\) plane. For example, when the reference voltage resides
in Sector I, two non-zero voltage vectors are \( V_1 \) and \( V_2 \), and the zero voltage vector is obtained as the combination of the smallest vectors, \( V_1 \) and \( V_3 \), in the timing diagram of the switching sequence. The time duration of \( V_1 \) and \( V_2 \) when the reference voltage vector is located in Sector I are obtained as

\[
T_1 = \frac{\sqrt{3}T}{2} \left[ (-\omega_t L_q i_q^* + \Delta v) \cos \hat{\theta}_r - (i_q^* R_s + \omega_c \lambda_f + K \Delta v) \sin \hat{\theta}_r \right], \tag{11}
\]

\[
T_2 = \frac{T}{2} \left[ (i_q^* R_s + \omega_c \lambda_f + K \Delta v) \cos \hat{\theta}_r - (\omega_t L_q i_q^* - \Delta v) \sin \hat{\theta}_r \right], \tag{12}
\]

where \( T \) is the switching period, and \( \hat{\theta}_r \) is the estimated rotor electrical position. The time durations that are used in the SVPWM scheme of the proposed FSTP inverter based sensorless scheme for phase-\( b \), phase-\( c \), and zero vectors are also calculated using Equations (11) and (12), respectively, as follows:

\[
T_b = T - T_1 - (T_0 / 2); \quad T_c = T_b - T_2; \quad T_0 = T - T_1 - T_2. \tag{13}
\]

The timing calculations can be obtained in a similar fashion for the rest of the sectors as well for the proposed sensorless control strategy. As can be seen in the time duration calculations, \( K \) gain has an influence on defining the duty cycle values of the switching actions in the proposed scheme. Since only two duty cycle values \( T_0 \) and \( T_2 \) given in Equation (13) are required in the proposed FSTP inverter based sensorless scheme, SVPWM complexity is minimized as opposed to the six-switch counterpart. Moreover, with less duty cycle components, dead-time compensation strategies can be simply implemented using the proposed sensorless scheme in the FSTP inverter compared to the SSTP inverter.

The overall stability of the proposed position sensorless speed control of PMSM scheme driven by an FSTP inverter under multiple simultaneous parameter variations (\( R_s \) and \( \lambda_f \)) is improved by proper selection of \( K \) gain in Equation (7). The output of the \( q \)-axis current controller, which is the electrical angular estimated speed \( \omega_e \), depends on the \( K \) gain that enables the system to respond dynamically and provides the system to protect its stability especially at low speeds [73]. The feedforward used in this work is actually the voltage estimator. The \( K \) gain is the gain matrix which stabilizes the estimator. An appropriate \( K \) gain must be selected to achieve a stable loop. Therefore, irrespective of other parameters, \( K \) gain is tuned to be five for this motor. The selected value of the \( K \) gain changes for various different motors. The low selected \( K \) gain value is effective while parameters do not change; however, under high parameter variations, high \( K \) gain value provides stable operation. At start-up, the \( K \) gain value is selected to be one not having an oscillation and, when the motor reaches the steady-state after ramping, its value is changed from one to five in a ramp during a specified time; therefore, the overall system is not affected from parameter variations. The proper maximum \( K \) gain that stabilizes the system under multi parameter detuning can be varied for other motors as seen in various observers. The selection criteria of \( K \) gain under heavy multiple parameter detuning in Equation (7) are investigated through experiments in Section 3. A complete block diagram for the proposed position sensorless PMSM drive scheme based-on stator feedforward voltage control (FFVC) using a four-switch space vector PWM (SVPWM) three-phase VSI is illustrated in Figure 5. The electrical angular speed \( \omega_e \) which is the output of the \( q \)-axis current controller is passed through a low-pass filter to obtain the estimated rotor speed \( \hat{\omega}_r \) in a similar fashion as the phase-lock loop (PLL), as shown in Figure 5.
2.3. Problem Formulation of the Proposed Method

The novelty of the proposed position sensorless speed control technique lies with the fact that it is the first contribution to the literature regarding the stator feedforward voltage control (FFVC) based position sensorless control of a PMSM drive that is insensitive to multi-parameter variations using a four-switch three-phase inverter under full load conditions at a low to nominal speed range. The stator feedforward voltage control (FFVC) algorithm for a four-switch three-phase (FSTP) inverter based PMSM is developed for an effective sensorless drive scheme. To develop the stator feedforward voltage control (FFVC) algorithm, the term $\Delta v$, the $d$-axis current controller output, is used in the steady-state $q$-axis stator feedforward voltage equation is multiplied by a $K$ gain and added to the $q$-axis steady-state $d$-axis voltage equation such that the $K\Delta v$ term represents the dynamic behavior in the $q$-axis voltage equation. Therefore, the $K\Delta v$ term holds the function of minimizing the errors in the PI regulator under dynamic changes in parameters and disturbance. Similarly, the $\Delta v$ term also acts as the derivative representation in a steady-state $d$-axis voltage equation for achieving a better transient response in the sensorless operation. Moreover, even though the proposed FFVC method is a closed-loop sensorless FOC, it is similar to $V/f$ control that is commonly used for induction motors; therefore, starting PMSM from zero speed is feasible. This was not practically possible before with the sensorless schemes that relied on the estimation of back-EMF such as classical Sliding Mode Observer (SMO) based position sensorless techniques. To show the superiority of the proposed method, it is compared with the classical back-EMF estimation method called Sliding Mode Observer (SMO). It is shown in the experimental study that the proposed sensorless scheme takes only 0.5 $\mu$s of processing time compared to the quite fast back-EMF sensing method called SMO. It is also believed that the...
ANN method given in [64] is difficult to implement and takes much longer processing time compared to our proposed scheme. Advantages and disadvantages of the proposed scheme with the existing well-known sensorless techniques are depicted in Table 1. In this paper, it is demonstrated that the parameter sensitivity is tremendously reduced by properly selecting the highest possible gain of the $\delta$-axis current regulator output used in the $q$-axis stator feedforward voltage control equation and therefore proper operation of the position sensorless FSTP based PMSM drive scheme is feasible even at considerably low to medium speed range.

**Table 1. Comparison of the proposed and existing sensorless methods.**

| Methods                      | Advantages                                      | Disadvantages                                      |
|------------------------------|-------------------------------------------------|----------------------------------------------------|
| Proposed                     | Simple, Fast Execution Time, Dynamic Response,   | Poor Performance in Standstill and Very Low Speed  |
|                              | Insensitive to Parameter Variation,              | under Load                                         |
|                              | No-load Start-up, No Chattering                  |                                                   |
| HFSI (High Frequency Signal  | Best at Very Low Speed, Capable of Hybridization,| Difficult to Implement, Noise at Medium            |
| Injection)                   | Independent of Motor Parameter Variations       | and High Speed, Low Dynamic Performance, Large     |
|                              |                                                 | Current Harmonics, High Torque Ripple, High       |
|                              |                                                 | Electrical Losses, Saturation Problem              |
| SMO (Sliding Mode Observer)  | Simple, Robust, Fast Execution Time, Anti-       | Poor Performance in Standstill and Low Speed,      |
|                              | Interference Ability, Free From Motor            | Chattering Problem                                 |
|                              | Parameters                                       |                                                   |
| ANN (Artificial Neural       | Learn-Based System, Easy of Training,           | Poor Performance in Standstill and Very Low       |
| Network)                     | Independent of Motor Parameters                  | Speed, Long Execution Time, Complex, Difficult to  |
|                              |                                                 | Implement                                         |

3. Experimental Verification

The implementation of the proposed position sensorless control scheme of a four-switch three-phase (FSTP) PMSM drive has been evaluated using an experimental test-bed, shown in Figure 6. The proposed control algorithm is implemented using a floating-point TMS320F28335 DSP with 10 kHz switching frequency.

![Experimental test-platform](image)

**Figure 6. Experimental test-platform.**

3.1. Experimental Set-up

The experimental set-up consists of a hysteresis dynamometer set, an inverter, a PMSM with an optical incremental encoder integrated for monitoring purpose, an eZdsp® board (Spectrum Digital, Stafford, TX, USA) with a TMS320F28335 DSP chip, and an interface and signal conditioning cards. The voltage unbalancing is seriously increased when the capacitors are selected as small. The inverter generates a maximum 4.3 $\mu$s dead-time and has two 2200 $\mu$F caps. The value of the DC-link voltage is
selected to be 565 V, which is the nominal PMSM DC-link voltage. Normally, the optimal value of DC bus voltage should be higher than 565 V in four-switch inverters to compensate for the reduction in power compared to a six-switch inverter case. The specifications and parameters of the PMSM are illustrated in Table A1 in the Appendix A.

3.2. Experimental Results

In the experiments, digital proportional-integral (PI) controllers are used in the speed and current loops. The initial rotor position is set to a predetermined value for proper start-up. Since the proposed position sensorless algorithm relies on the back-EMF based method, it is not possible to start at full load. Therefore, the motor is ramped from 0 to 360 r/min in 2 s under no-load. No instability is observed in the experimental no-load start-up using the proposed position sensorless scheme, as shown in Figure 7. Due to low sampling rate of the Magtrol dynamometer data acquisition system (Buffalo, NY, USA), in all experiments, the rotor speed and load torque data are obtained by the high resolution DAC module. During the steady-state speed of 360 r/min, a nominal step load torque (2 N·m) injection and rejection are applied, respectively. The resultant speed and shaft torque are provided in Figure 8. The satisfactory transient speed response is achieved under full load injection, and rejection with a reasonable low frequency oscillation without parameter detuning with \( K \) gain is chosen as 1.

![Figure 7](image-url)  
Figure 7. Experimental no-load ramp speed response (referenced 0 to 360 r/min in 2 s) without parameter detuning when \( K = 1 \) (low).

In Figure 9, the experimental steady-state phase-\( a \) and –\( b \) current waveforms are presented at 360 r/min under full load without parameter detuning when \( K = 1 \). As can be seen in Figures 7–9, the proposed position sensorless method is able to drive the PM motor without any instability under full load injection and rejection assuming that there are no parameter variations in the PM motor when the \( K \) gain is chosen as 1. Due to slight misalignment and concentrated windings of the motor, phase currents show some harmonic signatures, as seen in Figure 9. Moreover, since the dead-time effect is not mitigated, the phase current waveform shows some additional distortion in particular at zero crossings and during positive and negative peaks. The effects of stator resistance \( R_s \) and rotor flux linkage \( \lambda_f \) variations on the overall performance of the proposed drive are also investigated. The machine is run with external resistance under heavy load for a certain time until the PM rotor flux linkage \( \lambda_f \) amplitude decreases 40% less than its original value. Because changing \( \lambda_f \) directly in the actual machine is a difficult task, the motor is heated up with external resistance under heavy load.
first to achieve 82.35% higher $R_s$ and 40% less $\lambda_f$; then, the back-EMF constant and the final $R_s$ are measured afterwards. The resultant phase-\(a\) and -\(b\) axes current waveforms are shown in Figure 10 when both $R_s$ and PM rotor flux linkage $\lambda_f$ values are detuned under full load (2 N·m). Although 90% higher currents are drawn by the motor as shown in Figure 10, which results in more losses than normal operation, the proposed position sensorless method is able to drive the PM motor even under multiple simultaneous high parameter variations without any stability problem.

![Figure 8](image1.png)

**Figure 8.** Experimental speed response when full load (2 N·m) rejection and injection are applied respectively under 360 r/min steady-state speed with $K = 1$ (low).

![Figure 9](image2.png)

**Figure 9.** Experimental steady-state (360 r/min) phase-\(a\) and -\(b\) current waveforms under full load (2 N·m) without parameter detuning when $K = 1$ (low).
Figure 10. Experimental steady-state (360 r/min) phase-a and –b current waveforms under full load (2 N·m) while $R_s$ increased by 82.35% and $\lambda_f$ is decreased by 40% with $K = 5$ (high).

If the PM rotor flux linkage $\lambda_f$ is estimated using observer like methods without estimating the remaining parameters ($R_s$ and $L_s$) almost simultaneously, the correct PM rotor flux linkage $\lambda_f$ value cannot be obtained when these remaining parameters vary greatly. It is shown in previous work that $L_s$ is not affected by the variation of PM rotor flux linkage [74,75]. However, it is also previously reported in [73,74] that $R_s$ is highly sensitive to PM rotor flux linkage $\lambda_f$ variations and vice versa. It is observed in the simulations that, when a classical full-order observer is used to estimate the PM rotor flux linkage $\lambda_f$ when $R_s$ is changed 82.35% higher than its nominal value, then the PM rotor flux linkage is estimated to be 68% higher than the actual value in the proposed position sensorless speed control scheme. Even though the correct PM rotor flux linkage estimation can be achieved in the drive scheme when $R_s$ is increased 82.35% higher than its actual value and $\lambda_f$ is decreased 40% lower than its original value at the same time, the peak motor phase current increases 90% more than the expected full loaded value under multiple parameter variations. Although observing the changed values correctly allows stable position sensorless speed control, it does not improve machine efficiency because the machine inherently draws more current when the parameters are highly detuned. Figure 11 illustrates the effect of sudden $R_s$ increase under low $K$ gain of 1 at $t = 28$ s. It is seen that when a step increase in $R_s$ is applied under full load at 360 r/min, instability in speed is observed, which is shown in Figure 11. The rotor speed oscillates around the reference speed after the switch is closed and, a few seconds later, the motor stalls. The performance of transient speed response at no-load startup and during steady-state load injection and rejection can be improved by carefully selecting $K$ gain and time constants in the speed PI regulator and speed estimator filter. The importance of $K$ gain in Equation (7) is observed in the low and medium speed range. When $K$ is selected as low, between 1 to 3, the low to medium speed position sensorless method fails under heavy parameter detuning; however, if it is high enough, between 4 to 7, stability of the position sensorless speed control scheme is maintained even under heavy multiple simultaneous parameter detuning in the low to medium speed range. The value of $K$ under parameter variation depends on the size of the PM motor, speed, DC-link value, amount of the parameter variations, nonlinearities of the overall system, etc.
The nominal speed (900 r/min) full load steady-state experimental test while $R_s$ is increased by 82.35% and $\lambda_f$ is decreased by 40% with $K = 5$ (high) given in Figure 12 shows a non-oscillatory stable speed response. Moreover, an experimental low speed steady-state (90 r/min) speed response is shown in Figure 13a where full load (2 N·m) rejection is performed at $t = 7.87$ s and full load injection is applied at $t = 23$ s, while $R_s$ is increased by 82.35% and 40% less rotor flux linkage compared to the actual value with $K = 5$ (high). This is the lowest stable speed under full load injection and rejection with heavy parameter detuning.

**Figure 11.** Experimental speed response under full load (2 N·m) with the steady-state 360 r/min speed reference when $R_s$ is increased stepwise by 82.35% at $t = 28$ s with $K = 1$ (low).

**Figure 12.** Experimental steady-state nominal speed (900 r/min) response under full load (2 N·m) with $K = 5$ (high) while $R_s$ is increased by 82.35% and $\lambda_f$ is decreased by 40%.
Figure 13. (a) Experimental transient and steady-state low speed (90 r/min); (b) phase currents’ response when full load (2 N·m) rejection and injection are performed at $t = 7.87$ s and $t = 23$ s respectively with $K = 5$ (high) while $R_s$ is increased by 82.35% and $\lambda_f$ is decreased by 40%.

Figure 13b shows phase-$a$ and -$b$ current waveforms during steady-state under full load and at no-load, load rejection and when load injection has occurred, respectively. The stability is retained with reasonably low frequency oscillations. The speed transient step-down test from 120 r/min to 90 r/min under rated load is achieved successfully with high parameter detuning without instability using the proposed scheme, as shown in Figure 14. The least possible speed under no-load without parameter detuning is achieved to be around 78 r/min with the proposed scheme, as shown in Figure 15 where full load injection and rejection tests have been performed at $t = 15$ s and $t = 29$ s, respectively. In Figure 16, the speed is ramp down from $+90$ r/min to $-90$ r/min in 8 seconds under heavy multi-parameter changes without instability. The speed response given in Figure 16 has a good transient behavior and exhibits small fluctuations in a steady-state. An experiment with the actual position and the estimated position in the steady-state under a nominal load at the lowest possible velocity is given in Figure 17 under heavy multi-parameter changes. It is seen in Figure 17 that the estimated position tracks the actual position quite well at 90 r/min under heavy multi-parameter detuning without instability.
Figure 14. Experimental transient speed test (120 r/min to 90 r/min) under full load (2 N·m) with $K = 5$ (high) while $R_s$ is increased by 82.35% and $\lambda_f$ is decreased by 40%.

Figure 15. Experimental lowest steady-state speed (78 r/min) response test under full load (2 N·m) injection and rejection with $K = 5$ (high) while $R_s$ is increased by 82.35% and $\lambda_f$ is decreased by 40%.

In brief, an appropriate $K$ gain which is shown in Table A2 in Appendix A must be selected to achieve a stable loop. Therefore, irrespective of other parameters, $K$ gain is tuned to be five for this motor. The selected value of the $K$ gain changes for various different motors. The low selected $K$ gain value is effective while parameters do not change much; however, under heavy parameter variations, high $K$ gain value provides stable operation. In experimental studies, at start-up, the $K$ gain value is selected to be one that does not have an oscillation and, when the motor reaches the steady state after ramping, its value is changed from one to five in a ramp during a specified time; therefore, the overall system is not affected from parameter variations. The proper maximum $K$ gain that stabilizes the system under multi parameter detuning can be different for other motors as seen in various observers.
Figure 16. Experimental transient speed reversal test (±90 r/min) under full load (2 N·m) with $K = 5$ (high) while $R_s$ is increased by 82.35% and $\lambda_f$ is decreased by 40% of its original value.

Figure 17. Experimental steady-state (90 r/min) measured and estimated rotor position waveforms under full load (2 N·m) with $K = 5$ (high) while $R_s$ is increased by 82.35% and $\lambda_f$ is decreased by 40% of its original value.

Since there is a no zero-voltage vector as in SSTPI, there exist more harmonics as well as oscillations in currents and voltages in FSTPI. Under insufficient DC bus voltage conditions, the targeted power level cannot be reached due to the ratio of the voltages between SSTPI and FSTPI, which is 1/3 to 2/3 and the low speed operation of FSTPI with the proposed method fails. Moreover, even if the DC bus voltage is increased, serious voltage and current oscillations and harmonics in the system are observed and the motor insulations might break. Normally, DC voltage in FSTP inverter should be $C_1 = C_2$ at ideal conditions; however, in the real system, it becomes $C_1 \neq C_2$ during steady-state operation. Therefore, based on the measurement time, differences are observed between peak values of phase-$a$ and $-b$ currents. Moreover, because the dead-time effect is not compensated, the phase current waveform exhibits some additional distortion especially at zero crossings and at around positive and negative peaks. When the applied frequency is 6 Hz (0.1 per-unit), the magnitude of the voltage fluctuation is obtained as 34.10 V with two 2200 µF DC-link capacitors. For example, if the fluctuation
voltage is desired to be 15 V at 0.1 per-unit speed, the rated capacitance value has to be selected as 5000 µF.

3.3. Comparison of the Proposed Method with Classical SMO

The proposed control scheme is compared with the well-known position sensorless control method called sliding-mode observer (SMO). Sliding mode observer (SMO) is a promising approach for position sensorless schemes because of its independence from system parameter variations, less sensitivity to external disturbance and interference, fast convergence and robustness [76–79]. The experimental results demonstrate that, as opposed to the classical sliding-mode control (SMO), the proposed position sensorless method is stable at low speed ranges under full load compared to classical SMO even under heavy parameter detuning. The rotor speed is attempted to be decreased more down to 90 r/min at $t = 24.32$ s during approx. 80% higher stator resistance than the actual value and 40% less rotor flux linkage compared to the original rotor flux as in the proposed scheme; however, SMO is not able to track the reference speed and the rotor speed eventually goes to zero, as seen in Figure 18. The implementation process time related to the proposed method and the classical position sensorless method i.e., SMOs are compared in Figure 19. It is shown that the proposed method consumes 0.5 µs less time compared to the classical back-EMF sensing method (SMO). In this paper, it is demonstrated that the parameter sensitivity is tremendously reduced by properly selecting the highest possible gain of the $d$-axis current regulator output used in the $q$-axis stator feedforward voltage control equation and therefore proper operation of the position sensorless FSTP based PMSM drive scheme is possible even at considerably low to medium speed range.

![Figure 18](image-url)

**Figure 18.** Experimental rotor speed waveform in a steady-state (120 r/min) and when the speed is stepped down to 90 r/min at $t = 24.32$ s during 82.35% higher stator resistance than the actual value and $\lambda_f$ is decreased by 40% of its original value using classical SMO.
4. Conclusions

In this paper, a position sensorless speed control method based on stator feedforward $dq$-axes voltage control (FFVC) has been proposed for low-cost four-switched three-phase (FSTP) PMSM drive. Compared to traditional sensorless methods, the proposed method is simpler, more effective, and leads to a lower implementation processing time. Moreover, with the proposed method, the FSTP driven PMSM can start-up from zero speed under no-load without requiring any additional open-loop start-up procedures.

It is shown in the experiments that selecting a possible high $K$ gain in the stator FFVC algorithm enhances the stability of the overall drive even under heavy multiple simultaneous parameter variations, making the overall position sensorless speed control scheme quite insensitive to multiple parameter variations.

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**Appendix A**

**Table A1.** Specifications and parameters of the Permanent Magnet Synchronous Motor (PMSM).

| Parameter                                    | Value         |
|----------------------------------------------|---------------|
| Number of poles                              | 8             |
| Line-to-neutral rms voltage (V) at 200 Hz    | 230           |
| Rated torque (N·m)                           | 2             |
| Rated speed (r/min) at 60 Hz (1 per-unit)    | 900           |
| Rated rms current (A)                        | 4             |
| Stator inductance (H)                        | 0.0033        |
| Stator resistance (Ω)                        | 3.4           |
| Rotor magnetic flux linkage (Wb)             | 0.095         |
| Moment of inertia (kg·m²)                    | 0.0075        |
Table A2. $K$ gain selection criteria.

| $K$ Value | Max. $R_s$ Variation | Speed Oscillation at Max. $R_s$ |
|-----------|-----------------------|--------------------------------|
| 1         | 4%                    | 20%                            |
| 2         | 14%                   | 17%                            |
| 3         | 27%                   | 12%                            |
| 4         | 58%                   | 7%                             |
| 5         | 80%                   | 1%                             |
| 6         | 54%                   | 12%                            |
| 7         | 38%                   | 15%                            |

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