A hydrodynamical model for the Fermi-LAT γ-ray light curve of blazar PKS 1510–089

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ABSTRACT

A physical description of the formation and propagation of working surfaces inside the relativistic jet of the blazar PKS 1510–089 are used to model its γ-ray variability light curve using Fermi-LAT data from 2008 to 2012. The physical model is based on conservation laws of mass and momentum at the working surface as explained by Mendoza et al. (2009). The hydrodynamical description of a working surface is parametrized by the initial velocity and mass injection rate at the base of the jet. We show that periodic variations on the injected velocity profiles are able to account for the observed luminosity, fixing model parameters such as mass ejection rates of the central engine injected at the base of the jet, oscillation frequencies of the flow and maximum Lorentz factors of the bulk flow during a particular burst.

Key words: galaxies: active – quasars: individual: PKS 1510–089 – gamma-rays: galaxies.

1 INTRODUCTION

Among all types of AGN, blazars (blazar class is defined as radio-loud sources conformed by the BL Lac objects and the flat-spectrum radio quasars – FSRQ; see e.g. Fossati et al. 1997; Ghisellini et al. 1998, and references therein) represent the most energetic class. They are known to have the most powerful jets (e.g. Lister et al. 2009) and also show a highly variable spectral energy distribution (SED) from the radio to the γ-rays wavelengths (see Abdo et al. 2010a; D’Ammando et al. 2011, and references therein).

The FSRQ PKS 1510–089 is known to be one of the most powerful astrophysical objects with a highly collimated relativistic jet that has shown apparent superluminal velocities between 20c to 46c and with a semi-angle aperture for the jet ~0.2 (Jorstad et al. 2005). Since the angle between the relativistic jet and the observer’s line of sight ~1:4–3°, the jet almost coincides with the observer’s line of sight (Homan et al. 2002; Marscher et al. 2010). PKS 1510–089 was one of the γ-ray sources detected by EGRET (Hartman et al. 1999). It has been monitored at high energies with AGILE (D’Ammando et al. 2008; Pucella et al. 2008; Lucarelli et al. 2012) and by Fermi-LAT and AGILE (Tramacere 2008; Ciprini & Corbel 2009; D’Ammando et al. 2009). It has also been studied with Major Atmospheric Gamma-ray Imaging Cherenkov Telescope (MAGIC) and High Energy Stereoscopic System (HESS; Wagner et al. 2010; Cortina 2012). The most prominent outbursts displayed by PKS 1510–089 were reported by Kataoka et al. (2008), Ciprini & Corbel (2009) and Orienti et al. (2013). The high activity observed in this source turns it into an ideal target for the physical study of its highly relativistic jet.

Precise models for the light curve (LC) produced by the outburst and flares from blazars are not done using directly the data variations observed in different wavelengths. Instead, models are applied to explain the behaviour of the SED (e.g. Abdo et al. 2010a; D’Ammando et al. 2011). Direct understanding of the LC requires a precise knowledge of the hydrodynamical behaviour of the relativistic flow. Mendoza et al. (2009, hereafter M09) have constructed a hydrodynamical model of the motion of a working surface inside a relativistic jet which is able to fit the observed LCs of long gamma-ray bursts (lGRBs). Since the jets in blazars are highly relativistic and their jet is nearly pointing towards the observer, similar to the jets observed in lGRBs, the physical ingredients of both phenomena can be considered the same but occurring at different physical scales of energy, sizes, masses, accretion rates, etc. (cf. Mirabel & Rodríguez 2002).

The blazar PKS 1510–089 is of tremendous importance since it exhibits extreme relativistic motions. As such, its energy curve must present luminosity variations and periods of extreme activity displayed as outbursts that, when physically modelled, can yield a better understanding of the physical parameters associated with the mechanism producing the observed luminosity.

In this Letter, we assume that the mechanism producing the observed LC in a typical IGRB is exactly the same that produces the variable LC of the blazar PKS 1510–089. We thus apply the...
hydrodynamical jet model presented in M09 to the LC variations displayed by the blazar PKS 1510–089 in the γ-ray domain, using public data obtained with the Fermi-LAT telescope. The Letter is organized as follows. In Section 2, we explain in general terms the data reduction process. In Section 3, we describe the characteristics of our hydrodynamic model. The fit done to the data with the hydrodynamic model is explained in Section 4. The results of our fits and the discussion of the main physical parameters obtained in the modelling are presented in Section 5. Throughout this Letter, we use a standard cosmology with parameters obtained in the modelling are presented in Section 5.

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2 Fermi-LAT DATA

The γ-ray fluxes were obtained in the range 0.2–300 GeV using the public data base of Fermi-LAT from 2008 August 08 to 2012 May 28. The data were reduced with the Fermi science tool package (see e.g. Atwood et al. 2009) in the same energy range, taking into account the diffuse Galactic background radiation, the instrument response matrix p7v6, and considering a zenith angle <105°. We also calculated the active time of the detector and the point spread function. The γ-ray LC was constructed modelling the flux with a power law of the form dN/dE = N_0(E/E_0)^γ, with γ = 2–3 in accordance with the results of Abdo et al. (2010b). The fluxes and errors obtained with this package are given in photons × cm⁻² s⁻¹. For further physical interpretation of the data, we have converted these fluxes and errors to MeV cm⁻² s⁻¹.

The photons considered for analysis were taken from a region centred on the coordinates of PKS 1510–089 with a radius of 15°. Fig. 1 shows the γ-ray LC, with a bin size of 1 d. We chose these bins, since the errors are larger using shorter bin sizes, complicating the analysis of the data and because particular outbursts can be adequately resolved.

From Fig. 1, it follows that the source displayed the historical maximum outburst in MJD 558 51, corresponding to 2011 October 17 and reported by Hungve, Dutka & Ojha (2011). Another important outburst occurred in MJD 548 99 (2009 March 9) and was observed with AGILE (D’Ammando et al. 2009). Several flares or outbursts can be observed in the LC. The most relevant events occurred in MJD 547 17 (2008 September 8), MJD 548 43 (2009 January 12), MJD 552 00 (2010 January 4; Benítez et al. 2011), MJD 557 30 (2011 June 18) and MJD 559 54 (2012 January 28).

This last event was also observed by AGILE (Verrecchia et al. 2012) and MAGIC (Cortina 2012). Note that Marscher et al. (2010) report extra flares <200MeV during the period 548 50–549 50 MJD, which are not seen in our > 200MeV selection.

3 A HYDRODYNAMICAL MODEL FOR THE LC OF PKS 1510–089

The formation of internal shock waves on a relativistic jet are commonly explained by different mechanisms, such as the interaction of the jet with inhomogeneities of the surrounding medium, the bending of jets and time fluctuations in the parameters of the ejection (see e.g. Rees & Meszaros 1994; Mendoza & Longair 2002; Jamil, Fender & Kaiser 2008; M09). In particular, the model by M09 is a hydrodynamical description that can be applied to shock waves inside relativistic jets. This semi-analytical model describes the formation of a working surface inside a hydrodynamical jet due to periodic variations of the injected flow. When fast flow overtake slow flow, an initial discontinuity is formed and a working surface (two shock waves separated by a contact discontinuity) is produced. The working surface travels along the jet and radiates away kinetic energy. The paper by M09 assumed that the efficiency converting factor is ~1 and that it is mostly emitted in the γ-ray band. As explained in Section 1, the blazar PKS 1510–089 behaves as a scaled typical IGRB and as such, the hypothesis used by M09 can be extended to this particular object. As we will discuss in Section 5, this assumption is coherent with the physical properties found from the model. Following M09, we assume that flow is injected at the base of the jet with a periodic velocity given by

\[ v(\tau) = v_0 + c \omega^2 \sin \omega \tau, \]  

where τ is the time in the rest frame of the source, the velocity \( v_0 \) is the ‘background’ bulk velocity of the flow inside the jet and \( \omega \) is the oscillation frequency. The positive constant parameter \( \omega^2 \) is chosen in such a way that oscillations of the flow are small so that the bulk velocity \( v(\tau) \) of the flow does not exceed the velocity of light \( c \). The mass ejection rate \( m(\tau) \) from the central engine which is injected at the base of the jet is assumed constant through a particular outburst event, but is allowed to vary from one outburst to another. The radiated energy of the flow as a function of time is calculated as the difference between the total energy \( E_0 \) injected at the base of the jet and the kinetic energy inside the working surface \( E_{\text{ws}} \). The luminosity \( L \) is thus calculated as the derivative of this radiated energy.
energy with respect to time. As described by M09, there are two ways of calculating this luminosity curve. The first method consisted in a semi-analytical procedure and the second is performed with a full hydrodynamical numerical model. The authors showed that the semi-analytical model is in good agreement with the full numerical simulation, and as such we model the LC of PKS 1510−089 using their semi-analytical approach.

The semi-analytical approach is based on the assumption that equation (1) is valid and as such, one needs to know (or find through fits to observational data) the values of $v_0$, $\eta^2$, $\omega$ and $\dot{m}$. Furthermore, the mass ejection rate $\dot{m}$ enters in the description of the problem through the luminosity relation: $L \propto \dot{m}c^2$. The average bulk velocity $v_0$ must come from observational data [for this particular source, D'Ammando et al. (2008) reports a value $\Gamma(v_0) = 18$]. With this, the model is left with three free parameters: $\eta^2$, $\dot{m}$ and $\omega$, which can be fixed by fitting the best theoretical LC to the observational data.

4 MODELLING THE $\gamma$-RAY LC

To model the LC of Fig. 1, we have selected the most conspicuous flares. The criterion used consists of selecting only those flares that are beyond 3$\sigma$ noise level according to the errors shown in the LC.
By doing so, it turns out that 38 relevant peaks were chosen for our fitting.

As explained in Section 3, the model has four free parameters. The velocity parameter \( v_0 \) for this particular object is such that its Lorentz factor is \( \Gamma(v_0) = 18 \). To calculate the measured luminosity \( L \) from the observed flux \( F \), we multiply the observed flux \( F \) by \( (1-\Gamma(v_0)/c\cos \theta) \), which for this particular case is \( D = 1919 \) Mpc and the angle \( \theta \sim 1.3-3.4 \) is the angle between the jet and the observer’s line of sight (cf. Section 1). We have selected a beaming index \( p = 3 \) in accordance with the results of Wu et al. (2011) for blazars and IGRBs.

The model presented by M09 is such that the theoretical luminosity and time are presented in a very particular system of units. To fit the best theoretical LC to the data, one needs to have a common system of units. To achieve this, we have normalized the ‘measured’ luminosity to its peak and the measured time to the full width at half-maximum (FWHM) of the measured LC. In order to compare with the theoretical model, the theoretical LC is also normalized to its peak and the time is normalized to the FWHM of the theoretical luminosity curve. Once both theoretical and measured LCs are in this common dimensionless system of units, this procedure allows us to fit the best theoretical LC by performing a \( \chi^2 \) statistical test to find the optimal parameter \( \eta \). Note that in this normalized system of units, the model only depends on one free parameter: \( \eta \). Once the value of \( \eta \) is found, we can rescale back to physical units and in such a rescaling, the parameters \( m \) and \( \omega \) are obtained, since according to M09, \( L \propto m c^2 \) and \( \omega \propto \omega^{-1} \). The luminosity fits are then transformed to the observed flux dividing them by \( 4\pi D_c^2 \omega^{-1} \).

The results of these fits are shown in Fig. 2. The obtained values of the physical parameters of the model for each particular modelled outburst are presented in Table 1.

There is a certain subclass of outbursts that we do not model. These outbursts, labelled 8, 10, 20, 27 and 32 in Fig. 1, do not have enough data to allow us an accurate modelling. The outburst labelled 11 seems to have a fall that develops into a constant value while the burst lasted \( \sim 50–500 \). Note that in this normalized system \( \sim 18 \), for a luminosity distance \( \Delta \), which is found, we can rescale back to physical units and

\[
\dot{m} \sim 10^{-11} – 10^{-2} \text{ M}_\odot \text{s}^{-1}, \quad \rho \sim 100 \text{ s}, \quad \Gamma \sim 50–500.
\]

Note that the maximum and minimum values of the Lorentz factor for a particular outburst take into account the observational errors of the LC. The real value lies in between those calculated ranges. The inferred high relativistic Lorentz factors associated with the motion of the bulk velocity of the flow inside the jet of PKS 1510–089 makes it an ideal candidate for the application of the hydrodynamical model of M09. This is why that physical model can be applied naturally to IGRB and in this particular case to the extreme relativistic motion of the jet in the blazar PKS 1510–089. The energy released in each outburst can be calculated by taking the integral of the luminosity with respect to time, which occurs typically over periods of a few days. The value of this released energy is \( \approx 10^{39} – 10^{40} \) J, which shows the tremendous energy released by each individual outburst. This energy is to be compared with the energy released in about 10 s by an IGRB which is \( \approx 10^{44} \) J.

The most energetic burst, labelled 30, injected at the base of the jet a total mass \( m = \dot{m} \Delta t \approx 10^{-3} \text{ M}_\odot \), while the burst lasted \( \Delta t \approx 15 \) d. Analysis of all bursts shows that the ejected mass interval is \( 10^{-5} – 10^{-3} \text{ M}_\odot \), for a time duration range \( 4 \text{ d} \leq \Delta t \leq 30 \text{ d} \).

### Table 1. Different physical quantities obtained for the outbursts modelled in this work. The background Lorentz factor of the bulk velocity of the flow was assumed to be 18.

| Date       | ID number | MJD +540 00 | \( n_\gamma / c \times 10^{-3} \) | \( \Gamma_{\text{max}} \) | \( \omega^{-1} \times 10^{-3} \) | \( m \) \( \times 10^{-3} \text{ M}_\odot \) \( \text{yr}^{-1} \) |
|------------|-----------|-------------|-----------------------------|-----------------|-----------------|-----------------|
| 08 Sep     | 1         | 722.66      | 1.500                        | 106             | 1.05            | 2.16            |
| 08 Sep     | 2         | 728.66      | 1.520                        | 143             | 0.50            | 2.87            |
| 08 Sep     | 3         | 731.66      | 1.510                        | 120             | 0.41            | 2.37            |
| 09 Jan     | 5         | 849.66      | 1.501                        | 107             | 0.34            | 4.18            |
| 09 Jan     | 6         | 855.66      | 1.533                        | 209             | 1.49            | 2.80            |
| 09 Mar     | 7         | 899.66      | 1.330                        | 48              | 0.94            | 3.04            |
| 09 Mar     | 9         | 908.66      | 1.460                        | 76              | 0.37            | 6.61            |
| 09 Apr     | 12        | 925.66      | 1.430                        | 66              | 1.27            | 2.60            |
| 09 Apr     | 13        | 948.66      | 1.515                        | 130             | 1.22            | 7.67            |
| 09 May     | 15        | 957.66      | 1.300                        | 45              | 0.88            | 3.85            |
| 09 May     | 16        | 967.66      | 1.523                        | 152             | 1.05            | 3.38            |
| 09 Dec     | 17        | 1182.66     | 1.534                        | 219             | 2.60            | 2.40            |
| 09 Dec     | 18        | 1186.66     | 1.400                        | 58              | 0.39            | 2.06            |
| 09 Dec     | 19        | 1191.66     | 1.488                        | 94              | 1.24            | 2.84            |
| 10 Jan     | 21        | 1205.66     | 1.510                        | 120             | 1.04            | 2.23            |
| 10 Jan     | 22        | 1209.66     | 1.493                        | 98              | 0.95            | 4.76            |
| 10 Mar     | 23        | 1274.66     | 1.430                        | 66              | 0.68            | 2.99            |
| 11 Jun     | 24        | 1739.66     | 1.460                        | 76              | 0.74            | 3.16            |
| 11 Jul     | 25        | 1745.66     | 1.527                        | 169             | 0.81            | 8.09            |
| 11 Jul     | 26        | 1766.66     | 1.469                        | 81              | 0.36            | 7.13            |
| 11 Aug     | 28        | 1783.66     | 1.380                        | 55              | 0.41            | 11.40           |
| 11 Oct     | 29        | 1848.66     | 1.460                        | 76              | 0.67            | 3.30            |
| 11 Oct     | 30        | 1853.66     | 1.541                        | 383             | 1.32            | 24.52           |
| 11 Nov     | 31        | 1867.66     | 1.522                        | 149             | 0.57            | 16.83           |
| 11 Nov     | 32        | 1875.66     | 1.531                        | 193             | 0.88            | 6.37            |
| 12 Dec     | 36        | 1972.66     | 1.220                        | 39              | 0.66            | 3.55            |
| 12 Mar     | 37        | 1982.66     | 1.350                        | 50              | 2.03            | 7.48            |
The variations of the injected flow at the base of the jet cause the formation of working surfaces that produce bursts of $\gamma$-rays in the structure of the jet. The physical mechanism producing the oscillations of the input flow, which allows fast fluid to overtake the slow one, leading to the formation of working surfaces, is beyond the scope of this Letter. However, steady flow deviations and oscillations in such complicated phenomena are expected since the accretion–ejection mechanism associated with a particular object is not necessarily expected to be of constant velocity and mass accretion–ejection rates.

It is important to note that the assumption of seeing a blazar as a scaled version of an iGRB is not new. In an early attempt to find a unified model of jet and central-engine power, Mirabel & Rodriguez (2002) made this identification. The more relativistic a blazar jet is, the more it will resemble an iGRB. The idea of having a unified physical model for all types of astrophysical jets was first suggested by the pioneering works for the astrophysical scaling laws of black holes by Sams, Eckart & Sunyaev (1996) and Rees (1998). The work presented in this Letter further strengthens arguments about a unified picture of all astrophysical relativistic jets.

PKS 1510−089 resulted to be an ideal target to test the model by M09 since it closely resembles an iGRB in some of its outbursts. Future tests of the model have to be done with a wide variety of LCs from a large collection of blazars and microquasars.

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