Kinetics of Chromium(III) Transport Through a Liquid Membrane Containing DNNSA as a Carrier

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Abstract: Kinetics of Cr(III) ions transport through a bulk liquid membrane containing dinonylnaphthalenesulfonic acid (DNNSA) as a carrier, flowing over aqueous phases, has been examined. Special attention has been paid to the effect of the membrane’s velocity flow on the chromium concentration decrease in a feed phase. For the description of relationships of chromium(III) concentration in particular phases with the time, a model based on the assumption of consecutive first-order reactions was proposed. Satisfactory compatibility of experiments and model results have been obtained both for the membrane flow velocities below 0.0034 m·s⁻¹ when the interfaces begin to fluctuate slightly and for low initial Cr(III) concentration in the feed phase.

Keywords: Transport kinetics of chromium(III), dinonylnaphthalenesulfonic acid (DNNSA), bulk liquid membrane.
1. Introduction

Liquid membranes (LM) have appeared quite recently as a new prospective separation method. LM soon became very popular in various fields due to their good selectivity and efficiency achieved by the presence of a mobile and selectively acting agent (a carrier). The most popular application of liquid membranes concerns the removal and recovery of metal ions from wastewaters [1-3].

Chromium is one of the most important metals used commonly both in various processes and in production of different products. Because of its high toxicity and limited resources chromium discharges into the environment are strictly regulated.

Simultaneously to the works improving conventional methods of chromium separation intensive research has been conducted on new methods (for example liquid membranes). Most of these studies are focused on chromium(VI) [4-6] because of its hazardous properties. Chromium(III), as a non-toxic form, is largely ignored by the most researchers, but a high concentration of chromium(III) not only has a negative influence on living organisms but also oxidizes, in the environment, to chromium(VI) [7,8].

The results of our investigation of the kinetics of Cr(III) ion transport through a bulk liquid membrane containing dinonylnaphthalenesulfonic acid (DNNSA) as a carrier, flowing over aqueous phases, are presented in this paper.

2. Experimental Section

All experiments were performed in a system where aqueous phases flow over the membrane. The scheme of the experimental setup is shown in Figure 1.

Figure 1. Scheme of the measuring set with flows bulk liquid membrane. 1 – magnetic stirrers, 2 -sampling. M – membrane, F – feed phase, S – stripping phase, P1, P2 –pumps.
It consists of two separate Plexiglass vessels containing aqueous phases. The feed phase (F) was a chromium chloride solution (CrCl$_3$ analytical grade, POCh) with an initial Cr(III) concentration of $C_F = 0.019$, 0.038 and 0.058 M and pH = 4. The pH was adjusted with 0.1 M NaOH (NaOH analytical grade, Chempur). The stripping phase (S) was an aqueous 4 M H$_2$SO$_4$ (95% H$_2$SO$_4$ analytical grade, Chempur) solution. The volumes and the interfaces of both phases were the same and equal: $V = 400$ cm$^3$, $F = 56$ cm$^2$. Aqueous phases were mixed by magnetic stirrers (1) at a rotation rate of 50 rpm.

The liquid membrane (M) was an organic phase containing the dinonylnaphthalenesulfonic acid (DNNSA, Fluka) as a carrier dissolved in a mixture of kerosene and o-xylene. The concentration of DNNSA was $C_{DNNSA} = 0.2$ mol·dm$^{-3}$. The membrane circulated between the vessels with velocity of flow $v = 0.0027$, 0.0034 and 0.0049 m·s$^{-1}$. The flow of the liquid membrane was forced by peristaltic pumps (P1, P2) ensuring good mixing of the membrane. For the better flow stability of the membrane the overflow weirs to the vessels were fixed. The physico-chemical parameters of each phase were investigated earlier [9] and in the experiment the optimal ones were used.

The samples of aqueous phases were taken out by sockets (2) and chromium concentration was determined with a SPEKOL 220 spectrophotometer at a wavelength of 595 nm. The corresponding chromium concentration in the membrane was established from the material balance. The measuring setup was placed in thermostat and all experiments were performed at 25 ± 1°C.

3. Results and Discussion

3.1. Theoretical

The extraction reaction on the feed side (F) interface of a liquid membrane (M) can be written as follows [10]:

$$\text{Cr}^{3+}_{(F/M)} + 3\text{RSO}_3\text{H}_{(M/F)} \leftrightarrow (\text{RSO}_3)_3\text{Cr}_{(M/F)} + 3\text{H}^+_{(F/M)} \quad (1)$$

and the reaction on the stripping side interface of the liquid membrane in the presence of H$_2$SO$_4$ assumes the following form:

$$(\text{RSO}_3)_3\text{Cr}_{(M/S)} + 3\text{H}^+_{(S/M)} \leftrightarrow \text{Cr}^{3+}_{(S/M)} + 3\text{RSO}_3\text{H}_{(M/S)} \quad (2)$$

According to these reactions the transport of chromium(III) is coupled by countercurrent transport of H$^+$ ions. The mechanism of coupled countercurrent transport of Cr(III) ions through the membrane is schematically presented in Figure 2.

The variation of chromium(III) concentration in individual phases vs. time (as shown in a later Section) suggests that the ion transport obeys the kinetic laws of two consecutive irreversible first-order reactions according to the scheme:

$$\text{Cr(III)}_F \xrightarrow{k_F} \text{Cr(III)}_M \xrightarrow{k_S} \text{Cr(III)}_S$$

where: Cr(III)$_F$, Cr(III)$_M$, Cr(III)$_S$ – are the chromium(III) ions in the feed, membrane and stripping phases, respectively, and $k_F$, $k_S$ - are the pseudo-first-order apparent membrane entrance and exit rate constants, respectively.

It is evident that the presence of the proton gradient drives the whole transport process to completion without any back leakage of chromium(III) ions.
Figure 2. Schematic description of coupled counter transport of Cr(III).

Using the reduced concentrations: 

\[ R_F = \frac{C_F}{C_p}, \quad R_M = \frac{C_M}{C_p}, \quad R_S = \frac{C_S}{C_p} \]

where: \( C_F, C_M, C_S \) - chromium concentration appropriate in a feed, membrane and stripping phase, \( C_p \) – initial chromium concentration in a feed phase;

The above kinetic scheme may be described by the following set of equations [11]:

\[
\frac{dR_F}{dt} = -k_F \cdot R_F \tag{3}
\]

\[
\frac{dR_M}{dt} = k_F \cdot R_F - k_S \cdot R_M \tag{4}
\]

\[
\frac{dR_S}{dt} = k_S \cdot R_M \tag{5}
\]

Since \( k_F \neq k_S \), after integration of those equations, we get:

\[ R_F = \exp\left(-k_F \cdot t\right) \tag{6} \]

\[ R_M = \frac{k_F}{k_S - k_F} \cdot \left[ \exp\left(-k_F \cdot t\right) - \exp\left(-k_S \cdot t\right) \right] \tag{7} \]

\[ R_S = 1 - \frac{1}{k_S - k_F} \cdot \left[ k_S \cdot \exp\left(-k_S \cdot t\right) - k_F \cdot \exp\left(-k_F \cdot t\right) \right] \tag{8} \]

\( R_F \) decreases mono-exponentially with time, whereas the time variation of both \( R_M \) and \( R_S \) is bi-exponential. Additionally \( R_M \) has a maximum (for \( \frac{dR_M}{dt} = 0 \)) which allows for calculation of maximum values of time and chromium concentration in the membrane, according to the following equations:
\[ (C_M)_{\text{max}} = C_P \cdot \left( \frac{k_F}{k_S} \right) \frac{k_S}{k_S - k_F} \]  
\[ t_{\text{max}} = \frac{\ln \frac{k_S}{k_F}}{k_S - k_F} \]  

Differentiating the eqs. (6-8) the entrance (\( J_F \)) and exit (\( J_S \)) fluxes may be calculated. They are described by the following equations:

\[ J_F = \frac{V_F}{F_{F/M}} \cdot k_F \cdot C_P \cdot \exp(-k_F \cdot t) \]  
\[ J_S = \frac{V_S}{F_{M/S}} \cdot \frac{k_F}{k_S - k_F} \cdot C_M \cdot \left( \exp(-k_F \cdot t) - \exp(-k_S \cdot t) \right) \]  

At \( t = 0 \), when the concentration of chromium in the feed phase is equal to the initial concentration \( C_F = C_P \) the flux \( J_F \) assumes the following form:

\[ J_F = \frac{V_F}{F_{F/M}} \cdot k_F \cdot C_P \]  

The value of the flux \( J_S \) at \( t = t_{\text{max}} \), when the concentration of chromium in the membrane reaches its maximum \( C_M = C_{\text{max}} \), can be calculated from the equation:

\[ J_S = \frac{V_S}{F_{M/S}} \cdot k_S \cdot (C_M)_{\text{max}} \]  

3.2. Effect of the velocity of the membrane’s flow

Changes of chromium(III) concentration in particular phases with time for different flow velocities of membrane and its comparison with theoretical prediction are shown in Figure 3.

**Figure 3.** Changes of chromium(III) concentration in particular phases with time for three different flow velocity of the membrane: (a) \( w = 0.0027 \) m·s\(^{-1}\), (b) \( w = 0.0034 \) m·s\(^{-1}\), (c) \( w = 0.0049 \) m·s\(^{-1}\) and initial chromium concentration \( C_P = 5.8 \cdot 10^{-5} \) mol·m\(^{-3}\) ( ▲  - \( R_Z \), ■  - \( R_m \), ●  - \( R_S \), □  - eqs.6-8).
The transport of Cr(III) should involve three basic routines: (1) – the mass transport in the “bulk” phase (convection via stirring), (2) – the mass transport near the interface (the diffusion across the diffusion layer) and (3) – the interfacial reaction. The effect of the mass transport in the “bulk” phase can be neglected if the stirrer rotation speed of the aqueous phase is high enough and thus the bulk concentration of Cr(III) is uniform every time. It is also expected that a stronger mixing can decrease the thickness of the diffusion layer and thus increase the kinetics reliance on the interfacial chemical reaction.

Figure 4 indicates that the flow velocity of the membrane affects transport rates of the Cr(III) ions through the membrane. The constant $k_F$ increases nearly linearly with the increase of the membrane flow velocity for the investigated range of velocity. It suggests that the diffusion is the limiting step in the feed-membrane transport of Cr(III). The constant $k_S$ is nearly constant for the investigated range of the velocity. These results show that the chemical reaction is the limiting step in the membrane-stripping transport of chromium(III) ions.
Figure 4. The pseudo-first-order apparent membrane entrance ($k_F$) and exit ($k_S$) rate constants for different membrane flow velocity (initial chromium concentration $C_p = 5.8 \cdot 10^{-5} \text{ mol}\cdot\text{m}^{-3}$).

For all cases the stripping of chromium(III) was established as a limiting step of the process ($k_S < k_F$). With the increase in differences between transport kinetics of chromium(III) on both sides of the membrane an increase in chromium concentration in the membrane was observed. During almost the same time interval the increase in chromium concentration in the membrane was higher for the faster flow over the membrane. Increase of chromium concentration in the membrane caused an increase of maximum entrance ($J_F$) flux which is presented in Figure 5. The results presented indicate that a flow of the membrane over the liquid phases with velocity close to 0.0034 m·s$^{-1}$ had favorable influence on efficiency of a transport of chromium(III) in the studied system. Higher flow velocity of membrane caused instabilities of the liquid-liquid interfaces.

Figure 5. Variation of the entrance ($J_F$) and exit ($J_S$) fluxes with membrane flow velocity for initial chromium concentration $C_p = 5.8 \cdot 10^{-5} \text{ mol}\cdot\text{m}^{-3}$. 
3.3. Effect of initial chromium(III) concentration in the feed phase

The results of experimental data demonstrated variation of chromium concentration in the individual phases in the system with the flow of the membrane over aqueous phases vs. time for different initial chromium(III) concentration in the feed phase are in an agreement with a theoretical prediction for the velocity of the membrane equal \( w = 0.0034 \text{ m}\cdot\text{s}^{-1} \) (Figure 6).

**Figure 6.** Variation of chromium(III) concentration at individual phases with time for a different initial chromium(III) concentration into the feed phase: (a) \( 1.9 \cdot 10^{-2} \text{ mol}\cdot\text{dm}^{-3} \); (b) \( 3.8 \cdot 10^{-2} \text{ mol}\cdot\text{dm}^{-3} \); (c) \( 5.8 \cdot 10^{-2} \text{ mol}\cdot\text{dm}^{-3} \). Velocity of the membrane’s flow \( w = 0.0034 \text{ m}\cdot\text{s}^{-1} \) (▲ - \( R_Z \), ■ - \( R_m \), ● - \( R_S \), - eqs.6-8).
Decrease in initial chromium concentration in the feed phase causes high increase in extraction efficiency. For initial chromium concentration equal $C_p = 1.9 \cdot 10^{-5} \text{ mol} \cdot \text{m}^{-3}$ the high degree of chromium extraction (92%) was reached during a short time of ca. 5 hours. Additionally at the lower initial chromium(III) concentration in the feed phase the sharply growth of Cr(III) ions concentration into the stripping phase was observed. Moreover the low chromium concentration and a mixing of the membrane caused by its flow counteracted the accumulating of chromium inside the membrane.

**Figure 7.** Variation of: (a) the pseudo-first-order apparent membrane entrance ($k_F$) and exit ($k_S$) rate constants and, (b) the entrance ($J_F$) and exit ($J_S$) fluxes with initial chromium concentration in the feed phase for membrane flow velocity $w = 0.0034 \text{ m} \cdot \text{s}^{-1}$. 

(a)
As shown in Figure 7, the increase in initial chromium concentration in the feed phase clearly caused a reduction of the chromium extraction rate from the feed to the membrane phase. The rate of stripping is changed insignificantly. As a result the ratio of extraction and stripping rates decreases. But the stripping is still a limitation step of the process in the investigated range of initial chromium(III) concentrations in the feed phase.

There are some reasons of that. The hydrolyzed form of chromium(III) is extracted better by complexing agent [9] but the hydrolysis level decreases with an increase in initial chromium(III) concentration in the solution [12]. Additionally, during the first hour of the process, a sharp pH decrease was observed in the feed phase (Figure 8).
This was a consequence of the high proton gradient drive and this is in accordance with equation (1). In the solution with low pH, below 2, chromium(III) exists only in the Cr\(^{3+}\) form [12]. Probably this chromium(III) form is much less attractive for the DNNSA-carrier than hydrolyzed forms of chromium(III). The kinetics of process drop as a consequence. Moreover, as suggested by Coelho et al. [13] because tangential surface tension acts in the system it is possible for water to protrude into the organic phase, facilitating H\(^+\) ion transport across the membrane. This reduces the driving force and causes a sharp decrease in the process rate, so transport of chromium proceeded in two stages as has been presented earlier [14]. The existence of aqueous protrusions does not mean that the liquid membrane has collapsed. It was not possible because the thickness of the organic phase was equal to ca. 10 mm.

4. Conclusions

For the description of dependence of chromium(III) concentration in particular phases vs. time, in the system with the flowing liquid membrane, a model based on the assumption of consecutive first-order reactions was proposed. Satisfactory compatibility of experiments and model results were stated for cases when the velocity of the membrane flow was in the range of 0.0027 – 0.0049 m/s and the initial chromium(III) concentration in the feed phase was below \(C_F = 3.8 \times 10^{-5} \text{ m/s}^1\). Decrease in the velocity of the membrane-flow and increase in the initial chromium(III) concentration in the feed phase caused decrease in the rate and efficiency of the ion transfer. Additionally, the discrepancy between the experimental data and theoretical predictions increased.

References

1. Ashraf, M.; Chaudry, S.; Ahmad, M.; Malik, T. Supported liquid membrane technique applicability for removal of chromium from tannery wastes. *Waste Management* 1998, 17, 211–218.
2. Gill, J.S.; Singh, H.; Gupta, C.K. Studies on supported liquid membranes for simultaneous separation of Fe(III), Cu(II) and Ni(II) from dilute feed. *Hydrometallurgy* 2000, 55, 113–116.
3. Kulkarni, P.S.; Mulchopadhyay, S.; Bellary, M.P.; Ghosh, S.K. Studies on membrane stability and recovery of uranium(VI) from aqueous solutions using a liquid emulsion membrane process. *Hydrometallurgy* 2002, 64, 49–58.
4. Susmi, B.; Siddhartha, D.; Shyamal K.S. Mass transfer analysis of the extraction of Cr(VI) by liquid surfactant membrane. *Sep. Sci. Technol.* 2000, 35, 483–501.
5. Bhowal, A.; Datta, S. Studies on transport mechanism of Cr(VI) extraction from an acidic solution using liquid surfactant membranes. *J. Membr. Sci.* 2001, 188, 1–8.
6. Gęga J.; Walkowiak W. Separation of Cr(VI) and Cr(III) ions from sulfuric acid solutions with TOPO by bulk and supported liquid membranes. *Pol. J. Applied Chem.* 1999, XLIII (3-4), 147–160.
7. Schroeder, D.; Lee, G.F. Potential transformations of chromium in natural waters. *Water, Air, Soil Pollut.* 1975, 4, 355–365.
8. Świetlik, R. Kinetic study of redox processes of chromium in natural river water. *Pol. J. Env. Studies* **2002**, *11*, 165–169.

9. Lanagan, M.D.; Ibana, D.C. The solvent extraction and stripping of chromium with Cyanex 272, *Miner. Eng.* **2003**, *16*, 237–245.

10. Kuvaeva, A.I.; Mikulich, A.V.; Skripchenko, A.S. Extraction of chromium(III) ions with polynonylnaphthalenesulphonic acid solution. *Ser. Him. Navuk.* **1991**, *3*, 7–9.

11. Szpakowska, M.; Nagy, O’B. Membrane material effect on copper coupled transport through liquid membrane. *J. Membr. Sci.* **1991**, *64*, 129–143.

12. Kocaoba, S.; Akcin, G. Removal and recovery of chromium and chromium speciation with MINTEQA2. *Talanta* **2002**, *57*, 23–30.

13. Coelho, I.M.; Moura T.F.; Crespo, J.P.S.G.; Carrondo, M.J.T. Transport mechanisms in liquid membranes with ion exchange carrier. *J. Membr. Sci.*, **1995**, *108*, 231–244.

14. Gawroński, R.; Religa, P. Transfer of chromium(III) ions in systems with liquid membrane. In *Monograph of Environmental Engineering Committee of Polish Academy of Sciences*; PAN: Warsaw, Poland, 2004; Volume 22, pp. 295–304.

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