Enhanced Higgs boson production and avoidance of
CP-violation and FCNC in the MPP inspired 2HDM

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Abstract. The multiple point principle (MPP) can be used to suppress non-diagonal flavour
transitions and CP violation in the two Higgs doublet extension of the standard model. We
discuss the quasi-fixed point scenario in the MPP inspired two Higgs doublet model which leads
to the enhanced production of Higgs particles at the LHC if the MPP scale $\Lambda \simeq 10 - 100$ TeV.

1. Multiple point principle and custodial symmetries

The violation of CP invariance and the existence of tree-level flavor-changing neutral currents
(FCNC) are generic features of $SU(2)_W \times U(1)_Y$ theories with two Higgs doublets. Indeed the
couplings $m_3^2$, $\lambda_5$, $\lambda_6$ and $\lambda_7$ in the Higgs potential of the two-Higgs doublet model (2HDM)

$$V = m_1^2 |H_1|^2 + m_2^2 |H_2|^2 - \left[ m_3^2 H_1^\dagger H_2 + h.c. \right] + \frac{\lambda_1}{2} |H_1|^4 + \frac{\lambda_2}{2} |H_2|^4 + \lambda_3 |H_1|^2 |H_2|^2$$

$$+ \lambda_4 |H_1^\dagger H_2|^2 + \left[ \frac{\lambda_5}{2} (H_1^\dagger H_2)^2 + \lambda_6 |H_1|^2 (H_1^\dagger H_2) + \lambda_7 |H_2|^2 (H_1^\dagger H_2) + h.c. \right]$$

(1)

can be complex inducing CP-violation. Although one can eliminate the violation of CP
invariance and tree-level FCNC transitions by imposing a discrete $Z_2$ symmetry, such a
symmetry leads to the formation of domain walls in the early Universe which would create
unacceptably large anisotropies in the cosmic microwave background radiation.

Here we consider the multiple point principle (MPP) [1] as a possible mechanism for the
suppression of FCNC and CP-violation effects. MPP postulates the existence of the maximal
number of phases with the same energy density which are allowed by a given theory [1]. When
applied to the 2HDM the multiple point principle implies the existence of a large set of degenerate
vacua at some high energy scale $\Lambda$ (MPP scale) that can be parametrised as

$$< H_1 > = \begin{pmatrix} 0 \\ \Phi_1 \end{pmatrix}, \quad < H_2 > = \begin{pmatrix} 0 \\ \Phi_2 e^{i \omega} \end{pmatrix},$$

(2)

where $\Phi_1 = \Lambda \cos \gamma$, $\Phi_2 = \Lambda \sin \gamma$, $\tan \gamma = \lambda_1/\lambda_2$ while $\omega$ is an arbitrary parameter. According to
the MPP vacua at the electroweak and MPP scales must have the same vacuum energy density.

The degeneracy of the MPP scale vacua can be achieved only if the Lagrangian for the
Higgs-fermion interactions is invariant under symmetry transformations (see [2]):

$$H_1 \to e^{i \alpha} H_1, \quad H_2 \to e^{i \beta} H_2,$$
$$u_R \to e^{i \alpha} u_R', \quad u_R' \to e^{i \beta} u_R', \quad d_R \to e^{-i \alpha} d_R', \quad d_R' \to e^{-i \beta} d_R',$$
$$e_R \to e^{-i \alpha} e_R', \quad e_R' \to e^{-i \beta} e_R'.$$

(3)
where $u'_i$, $d'_i$, $e'_i$ are quark and lepton eigenstates which couple to $H_1$ while $u''_i$, $d''_i$, $e''_i$ are fermion eigenstates that interact with $H_2$. In Eq. (3) the subscript $R$ denote right-handed fermion fields. Two global $U(1)$ symmetries (3) forbid non–diagonal flavour transitions at the tree level. Moreover these symmetries lead to the vanishing of $\lambda_5$, $\lambda_6$ and $\lambda_7$ in the Higgs potential (1) that cause CP–nonconservation in the 2HDM. The mixing term $m^2_{A}(H_1^*H_2)$, which is not forbidden by the MPP, softly breaks custodial global symmetries but does not create new sources of CP–violation or FCNC transitions.

The degeneracy of the physical and MPP scale vacua requires Higgs and Yukawa couplings to be adjusted so that an appropriate cancellation among the quartic terms in the Higgs potential (1) takes place. Such cancellation becomes possible only if $\lambda_1(\Lambda) < 0$ and the combination of the Higgs self–couplings $\lambda = \sqrt{\lambda_1\lambda_2} + \lambda_3 + \lambda_4$ as well as its beta function $\beta_\lambda$ go to zero at the scale $\Lambda$ [3]. At moderate values of $\tan\beta = v_2/v_1$ where $v_2$ and $v_1$ are vacuum expectation values of $H_2$ and $H_1$ in the physical vacuum, the last two MPP conditions can be written as follows [3]

$$\lambda_3(\Lambda) = -\sqrt{\lambda_1(\Lambda)\lambda_2(\Lambda)} - \lambda_4(\Lambda),$$

$$\lambda^2_4(\Lambda) = \frac{6h^2_1(\Lambda)\lambda_1(\Lambda)}{(\sqrt{\lambda_1(\Lambda)} + \sqrt{\lambda_2(\Lambda)})^2} - 2\lambda_1(\Lambda)\lambda_2(\Lambda) - \frac{3}{8} \left(3g_3^2(\Lambda) + 2g_2^2(\Lambda)g_1^2(\Lambda) + g_4^4(\Lambda)\right),$$  \hspace{1cm} (4)

where $h_i(\Lambda)$ is the top quark Yukawa coupling. Thus $\lambda_3$ and $\lambda_4$ are not independent parameters in the considered model. As a result the MPP inspired 2HDM has less free parameters than the 2HDM of type II and therefore can be regarded as a minimal non–supersymmetric two Higgs doublet extension of the SM. It is also worth noting here that the MPP conditions (4) are satisfied identically in the MSSM above the supersymmetry breaking scale.

The MPP conditions (4) must be supplemented by the vacuum stability requirements, i.e. $\lambda_1, 2(\mu) > 0$ and $\lambda(\mu) > 0$, which have to be fulfilled everywhere from $\mu = M_t$ to $\mu = \Lambda$. Otherwise another minimum of the Higgs potential (1) with negative vacuum energy density arises at some intermediate scale, preventing the consistent realisation of the MPP in the 2HDM.

2. Higgs phenomenology

The renormalisation group (RG) flow of all couplings in the MPP inspired 2HDM is determined by $\lambda_1(\Lambda), \lambda_2(\Lambda)$ and $h_i(\Lambda)$. When $h_i(\Lambda) > 1$ the solutions of the RG equations for the top quark Yukawa coupling are concentrated in the vicinity of the quasi–fixed point at the electroweak scale. The value of $\tan\beta$ that corresponds to the quasi–fixed point scenario depends mainly on the MPP scale $\Lambda$. It varies from 1.1 to 0.5 when $\Lambda$ changes from $M_{Pl}$ to 10 TeV [4]. At large values of $h_i(\Lambda)$ the MPP and vacuum stability conditions constrain $\lambda_3(\Lambda)$ very strongly. Our numerical studies show that for $\Lambda = M_{Pl}$ and $\lambda_3(M_{Pl}) = \lambda_2(M_{Pl}) = \lambda_0$ the ratio $\lambda_0/h^2_i(M_{Pl})$ can vary only within a very narrow interval from 0.79 to 0.87 if $h_i(\Lambda) > 1.5$. This ensures the convergence of the solutions of the RG equations for $\lambda_i(\mu)$ to the quasi–fixed points.

The Higgs spectrum of the two Higgs doublet extension of the SM contains two charged and three neutral scalar states. Because in the MPP inspired 2HDM CP–invariance is preserved one of the neutral Higgs bosons is always CP–odd while the two others are CP–even. The qualitative pattern of the Higgs spectrum depends very strongly on the mass of the pseudoscalar Higgs boson $m_A$ (see Fig. 1). When $m_A \gg M_t$ the masses of charged, CP–odd and heaviest CP–even Higgs bosons are almost degenerate around $m_A$. In the considered limit the lightest CP–even Higgs boson mass $m_{h_1}$ attains its maximal value which is determined by $\lambda_i(\mu_t)$ and $\lambda_3(\mu_t)$.

For each MPP scale $\Lambda$ one can compute the values of the Higgs self–couplings at the electroweak scale and $\tan\beta$ near the quasi–fixed point. Because at large values of the pseudoscalar mass $m_{h_1}$ is almost independent of $m_A$, the upper bound on the lightest Higgs scalar mass depends predominantly on the scale $\Lambda$. When the MPP scale is high such dependence is relatively weak. If $\Lambda > 10^{10}$ GeV the mass of the lightest Higgs particle in the quasi–fixed
Figure 1. Spectrum of Higgs bosons near the quasi–fixed point versus $m_A$ for $\Lambda = 10$ TeV. The dash–dotted and dashed lines correspond to the CP–even Higgs boson masses while the solid line represents the mass of the charged Higgs states.

Figure 2. Absolute values of the relative couplings $R_{t\tilde{b}_i}$ of the Higgs scalars to the top quark in the quasi–fixed point scenario as a function of $m_A$ for $\Lambda = 10$ TeV. Solid and dashed–dotted curves correspond to the lightest and heaviest CP–even Higgs states.

The quasi–fixed point scenario does not exceed 125 GeV [4]. However at low MPP scales $\Lambda \simeq 10 – 100$ TeV the theoretical restriction on $m_h$, reaches 200 – 220 GeV. The lightest Higgs scalar in the considered case is predominantly a SM–like Higgs boson, since its relative coupling to a $Z$ pair is rather close to unity. Nevertheless at low MPP scales the quasi–fixed point scenario leads to large values of the relative coupling of the lightest Higgs scalar to the top quark resulting in the enhanced production of this particle at hadron colliders (see Fig. 2). Thus the analysis of production and decay rates of the SM–like Higgs boson at the LHC should make possible the distinction between the quasi–fixed point scenario in the MPP inspired 2HDM with low scale $\Lambda$, the SM and the MSSM even if extra Higgs states are relatively heavy, i.e. $m_A \simeq 500 – 700$ GeV.

3. Conclusions
We have argued that the MPP assumption allows us to suppress FCNC and CP violating phenomena in the 2HDM. When $h_t(\Lambda) > 1$ the solutions of the RG equations in the MPP inspired 2HDM converge to the quasi–fixed point, leading to stringent restrictions on the lightest Higgs scalar mass. In the quasi–fixed point scenario the Higgs couplings to the $t$–quark can be significantly larger than in the SM, which allows us to test this scenario at hadron colliders.

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References
[1] Bennett D L and Nielsen H B 1994 Int. J. Mod. Phys. A 9 5155
Bennett D L, Froggatt C D and Nielsen H B 1995 Perspectives in Particle Physics’94 ed D Klabučar, I Picek and D Tadić (Singapore: World Scientific) p 255 (Preprint hep-ph/9504294)
[2] Froggatt C D, Nevzorov R, Nielsen H B and Thompson D in preparation
[3] Froggatt C D, Laperashvili L, Nevzorov R, Nielsen H B and Sher M 2004 The two-Higgs doublet model and the multiple point principle Preprint hep-ph/0412333
Froggatt C D, Laperashvili L, Nevzorov R, Nielsen H B and Sher M 2006 Phys. Rev. D 73 095005
[4] Froggatt C D, Nevzorov R, Nielsen H B and Thompson D Fixed point scenario in the Two Higgs Doublet Model inspired by degenerate vacua Preprint hep-ph/0708.2903