Broadband Spin-Selective Wavefront Manipulations Based on Pancharatnam–Berry Coding Metasurfaces

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1. INTRODUCTION

Metasurfaces are composed of two-dimensional (2D) subwavelength artificial elements and have attracted much attention in recent years due to their powerful ability in the manipulations of electromagnetic (EM) waves.1−4 However, most of the traditional metasurfaces have no chirality, and thus they have the same amplitude and/or phase responses for both left- and right-handed circularly polarized (CP) waves.5,6 The proposal of Pancharatnam–Berry (PB) metasurfaces makes it possible to control the left- and right-handed CP waves independently because the introduction of the propagation and geometric phases can break the locked spin-flipped phase limitation.7−9 Many fantastic works have been proposed on the basis of PB metasurfaces, such as the broadband spin-decoupled reflector antenna,10 multichannel vectorial hologram,11−13 multiple-input multiple-output antenna with information encryption,14 near-field and far-field optical imaging,15,16 polarization-insensitive cloaking,17 and even helicity-delinked manipulations of surface waves.18

Chiral metamirrors as a special kind of metasurface,19,20 which can efficiently reflect the designated CP waves without reversing the spin state and simultaneously suppress its orthogonally polarized wave by absorption, have also attracted much attention. They are widely used in the spin-selective wavefront manipulation of EM waves, such as the spin-selective anomalous reflection,21,22 chiral multiplexing hologram,23 dual-band spin-selective absorber,24 and full-dimensional manipulation of optical waves.25 However, the previous chiral metamirrors are generally based on asymmetric resonant elements, which must meet the requirement of breaking n-fold (n > 2) rotational symmetries, and most of them can only exhibit chiral response in a narrow band. Reference 26 proposes that combining two asymmetric split-ring resonators into a supercell can increase a certain bandwidth of chiral response, whose full width at half maximum is 5.7%. Nevertheless, the absorption of such a supercell-based chiral metamirror is still attributed to the spin-selective induced resonance within the chiral elements, which leads to the limitation of absorption bandwidth.

Digital coding metasurfaces as a bridge linking between the physics world and digital information world has attracted much attention in recent years,7−9 which opens up a new avenue for the development of metasurfaces. In addition to the control of linearly polarized waves,28−30 the digital coding metasurfaces can also be used for the manipulation of CP waves, such as the multiple beams control,36 spin-to-orbital generation,38 spin-symmetry breaking,39 and even quantum information representation.40 However, most of the previous works only focus on simultaneously manipulating the wavefronts of left-handed and right-handed CP waves with the same reflection efficiency and a lack of discussion about spin-selective reflection, which may find some potential applications similar to the chiral materials, but having an obvious advantage in broad bandwidth.
In this paper, a new method based on the spin-decoupled PB coding metasurface has been proposed to achieve the broadband spin-selective wavefront manipulation. Different from the traditional chiral metamirror that is composed of chiral meta-elements, the proposed PB metasurface is composed of 2-bit coding nonchiral elements. By introducing both the geometric phase and propagation phase, the wavefront of left-handed CP (LCP) and right-handed CP (RCP) waves can be manipulated independently without reversing spin states. Hence, the spin-selective reflection with the arbitrary wavefront manipulation can be achieved by efficiently reflecting the designated CP wave (LCP or RCP wave) and at the same time randomly diffusing its orthogonal polarized wave (RCP or LCP wave). More importantly, because no resonant chiral meta-elements are used in this design, therefore the proposed spin-selective PB metasurfaces can work in a broad frequency band. A PB coding metasurface with the spin-selective anomalous reflection has been designed and measured, and the results show that the proposed PB coding metasurface has a good spin-selective performance in a broad band from 16 to 24 GHz. Meanwhile, the results also show that the proposed spin-selective PB coding metasurface also has the chiral-like characteristics, even though it is composed of nonchiral elements.

2. RESULTS AND DISCUSSION

2.1. Theoretical Analysis and Simulations. The schematic of the proposed PB coding metasurface is demonstrated in Figure 1a, which has the ability to anomalously reflect the designated CP wave without reversing the handedness, while simultaneously suppressing its orthogonal spin state. We arbitrarily assume that the LCP wave is efficiently reflected, while the RCP wave is suppressed by random diffusion.

The metasurface is composed of quasi-I-shaped structures, as demonstrated in Figure 1b,c, which is designed based on the printed circuit board technology. The thickness of covered copper is 0.018 mm with conductivity of $5.8 \times 10^7$ s/m. A grounded plane is on the back of the unit structure spaced by a dielectric substrate of F4BK265 (polytetrafluoroethylene) with thickness of $h = 2$ mm, whose relative permittivity is 2.65 and loss tangent is 0.001. The other parameters shown in Figure 1b,c are $P = 4.4$ mm, $w = 0.32$ mm, $r = 1.75$ mm, and variables $\alpha$ and $\beta$, where $\alpha$ is defined as the azimuth angle along the x axis and $\beta$ is defined as the angle of arc. In order to more easily show the performance of the unit structure, a new local coordinate is defined as $\omega_{0v}$, in which the axes $u$ and $v$ are parallel and vertical, respectively, to the metallic strip connected to two arcs.

Figure 2 shows the phase and amplitude responses of the unit varying with $\alpha$ and $\beta$, which are simulated by using commercial software CST Microwave Studio (CST Computer Simulation Technology GmbH, Darmstadt, Germany). The phase difference between the $u$- and $v$-polarized reflection waves can keep $180^\circ$ in a broad band for any $\beta$, such as $\beta = 48^\circ$, $92^\circ$, $124^\circ$, and $154^\circ$, as shown in Figure 2a, implying that the unit structures satisfy the requirement of PB phase. It is worth mentioning that the unit cell boundary condition is adopted in all simulations, as the inset shown in Figure 2b, while the plane wave excitation can be set as linearly and circularly polarized waves, respectively, according to the requirements. The reflection phases of CP waves varying with $\beta$ at different frequencies are demonstrated in Figure 2c, in which $\alpha$ is fixed as $0^\circ$. The results show that the reflection phases are almost linearly decreased as $\beta$ increases, and this $\beta$-dependent reflection phase ($\phi_{fl}$) is usually named as the propagation phase. The reflection phases of CP waves varying with $\alpha$ at different frequencies are demonstrated in Figure 2e, in which $\beta$ is fixed as $154^\circ$. The results show that the reflection phases are gradually increased for LCP waves and decreased for RCP waves as $\alpha$ increases, and this $\alpha$-dependent reflection phase ($\phi_{ru}$) is usually named as the geometric phase. In addition, the units can keep high reflection efficiency for the different cases as shown in Figure 2b–f.

In order to obtain the reflection phases of LCP and RCP waves, it can start from the relationship between the incident waves and reflection waves under the $xoy$ coordinate when the unit structure is rotated by an angle of $\alpha$, which can be expressed as

$$
[M \cdot R] = \begin{bmatrix} E_x' \\ E_y' \end{bmatrix} = \begin{bmatrix} E_{x1} \\ E_{y1} \end{bmatrix}
$$

in which $E_x'$ and $E_y'$ represent the $x$- and $y$-polarized components of the reflected waves, $E_{x1}$ and $E_{y1}$ represent the $x$- and $y$-polarized components of the incident waves, $M \cdot [\cos \alpha - \sin \alpha \sin \alpha \cos \alpha]$ is the rotation matrix, and $R = \begin{bmatrix} A_x \ e^{i\phi_{ru}} & 0 \\ 0 & A_y \ e^{i\phi_{ru}} \end{bmatrix}$ is the reflection matrix of the unit structure under the $\omega_{0v}$ coordinate; here $A_x = A_y = 1$ because all the incident waves are almost totally reflected, and $\phi_{ru} \approx \pi$ according to the results shown in Figure 2a. The LCP and RCP components can be expressed with the linear polarization components under the $xoy$ coordinate by

$$
\begin{bmatrix} E_{L1} \\ E_{R1} \end{bmatrix} = \begin{bmatrix} \frac{1}{\sqrt{2}} \left( 1 + i \right) \\ \frac{1}{\sqrt{2}} \left( 1 - i \right) \end{bmatrix} \begin{bmatrix} E_x' \\ E_y' \end{bmatrix}
$$

in which $E_x'$ and $E_y'$ represent the LCP and RCP components of the incident waves, and $E_{L1}$ and $E_{R1}$ represent the LCP and RCP components of the reflected waves. It is worth

![Figure 1](https://example.com/figure1.png)

**Figure 1.** Schematic of the EM responses of the proposed PB coding metasurface and its unit structure. (a) Metasurface can anomalously reflect the LCP wave without reversing the handedness, while suppressing the RCP waves by random diffusion in a broad frequency band. (b,c) Quasi-I-shaped structure.
mentioning that the LCP (and RCP) waves have the opposite rotation direction for the incident and reflected LCP (and RCP) waves because their transmission directions are also opposite. We define \( C = \frac{1}{\sqrt{2}} \begin{bmatrix} 1 & -i \\ 1 & i \end{bmatrix} \) and \( C' = \frac{1}{\sqrt{2}} \begin{bmatrix} 1 & -i \\ 1 & i \end{bmatrix} \), then combining eqs 1 and 2, there is

\[
\begin{bmatrix}
E_{LL}^i \\
E_{RR}^i
\end{bmatrix} = C' M R M^{-1} C^{-1}
\begin{bmatrix}
E_L \\
E_R
\end{bmatrix} =
\begin{bmatrix}
\epsilon e^{i(\varphi - 2\alpha)} & 0 \\
0 & \epsilon e^{i(\varphi + 2\alpha)}
\end{bmatrix}
\begin{bmatrix}
E_L^i \\
E_R^i
\end{bmatrix}
\]

Therefore, the reflection phases of LCP and RCP waves can be calculated by

\[
\begin{align*}
\varphi_{LL} &= \varphi_e - 2\alpha = \varphi_p - 2\alpha \\
\varphi_{RR} &= \varphi_e + 2\alpha = \varphi_p + 2\alpha
\end{align*}
\]

in which \( \varphi_e = \varphi_p \) is the propagation phase and \( \varphi_e = 2\alpha \) is the geometric phase. Hence, according to eq 4, the PB metasurfaces can independently control the reflection phases of LCP and RCP waves by changing \( \alpha \) and \( \beta \).

Four different unit structures with \( \beta = 154, 124, 92, \) and \( 48^\circ \) are selected to construct the 2-bit PB coding metasurface, whose propagation phases continuously increase with the interval of about \( 45^\circ \) when \( \beta \) decreases from 154 to \( 48^\circ \), as shown in Figure 2c. We note that the absolute phase values of these units will not affect the performance of the PB coding metasurface and therefore can be normalized to the reflection phase of digital code “00” (0°), which is an unit with \( \beta = 154^\circ \) and \( \alpha = 0 \). Then, the other spin-decoupled digital codes “01” (90°), “10” (180°), and “11” (270°) for both LCP and RCP waves can be achieved according to the eq 2. At last, 16 unit elements are used to construct the proposed PB coding
metasurface, as demonstrated in Figure 3. For simplicity, these units are named as “$C_L/C_R$”, in which $C_L$ and $C_R$ represent the digital states of LCP and RCP waves, respectively.

A 2-bit PB coding metasurface with the function of spin-selective anomalous reflection is designed and simulated by encoding the gradient phase code of LCP wave and the random phase code of RCP wave into a single metasurface, as shown in Figure 4a. The gradient phase coding pattern comprises eight phase periods along $x$ direction with the coding sequence of “00, 00, 01, 01, 10, 10, 11, 11”. The random phase coding pattern contains $8 \times 8$ equal-sized blocks and each block is composed of $4 \times 4$ 1-bit unit cells of “00” or “10”. Hence, eight unit elements of “00/00”, “00/10”, “01/00”, “01/10”, “10/00”, “10/10”, “11/00”, and “11/10” are used to construct the PB coding metasurface, as shown in Figure 4a, named as an L-type metasurface, which is composed of $32 \times 32$ pixels with an area of $140.8 \times 140.8$ mm². According to the

Figure 3. 2-bit spin-decoupled unit coding elements.

Figure 4. Characterization of the L-type gradient coding metasurface with the broadband spin-selective reflection. (a) Phase distributions for LCP and RCP waves and layout of the metamirror. (b,c) Full-wave simulated 2D and 3D (insets) far-field radiation patterns of the metamirror under the normal incidence of (b) LCP and (c) RCP waves.
Figure 5. Characterization of the R-type gradient coding metasurface with broadband spin-selective reflection. (a) Layout of the L-type and R-type metasurfaces. (b) Phase distributions of the R-type metasurface for LCP and RCP waves. (c,d) Full-wave simulated 2D and 3D (insets) far-field radiation patterns under the normal incidence of (c) LCP and (d) RCP waves.

Figure 6. Experimental setup and measurement results. (a) Photograph of the fabricated prototype of L-type gradient coding chiral metamirror. (b) Experimental setup in an anechoic chamber. (c,d) Measured far-field radiation patterns at different frequencies for (c) LCP and (d) RCP waves, respectively. (e,f) Co-polarization reflection coefficients for LCP and RCP as a function of frequency. (e) Simulation and (f) measurement.
knowledge of general Snell’s law, the angle of the anomalous reflection waves can be calculated by

\[ \theta_i = \sin^{-1}(\sin \theta_i + \lambda_0 / \Gamma) \]  

in which \( \theta_i \) is the reflection angle, \( \theta_0 \) is the incident angle, \( \lambda_0 \) is the working wavelength, and \( \Gamma \) is the physical length of one 2\( \pi \) phase period. In this design, \( \theta_i \) is equal to 0 (\( \theta_i = 0 \)) due to the normal incidence and \( \Gamma = 8 \times p = 35.2 \) mm; therefore, the reflection angle is only related to the working wavelength of \( \lambda_0 \).

Figure 4b,c shows the full-wave simulated far-field radiation patterns at different frequencies in the xoz plane, in which Figure 4b shows the results of LCP wave and Figure 4c shows the results of RCP wave, and the results are normalized by the reflection energy of a bare copper plate with the same dimension. The insets demonstrate the three-dimensional (3D) far-field radiation patterns of the metasurface at 20 GHz. The results show that the RCP waves are randomly diffused to achieve low RCS scattering, which are smaller than −12 dB at different frequencies. It is worth mentioning that the large sidelobes shown in Figure 4b are mainly caused by the large discrete phase distribution of 2-bit coding sequence, which achieve low RCS scattering, which are smaller than

\[ \text{RCS} \]  

−32, −28, −25, −23, and −20° at 16, 18, 20, 22, and 24 GHz, respectively, having a good agreement with the theoretical expectation.

Figure 5a shows the mirror of L-type metasurface, called as a R-type metasurface, whose phase coding patterns are mirrored with that of the L-type metasurface, as shown in Figure 5b. The full-wave simulation results of the R-type metasurface are demonstrated in Figure 5c,d, which shows that it has the completely opposite EM responses to that of the L-type metasurface. The LCP wave is suppressed by random diffusion, while the RCP wave is efficiently reflected with radiation angles of 32, 28, 25, 23, and 20° at 16, 18, 20, 22, and 24 GHz, respectively. It should be noted that the L-type and R-type metasurfaces cannot be coincided with each other through translation or rotation operation; therefore, the proposed PB coding metasurface also exhibits the chiral-like characteristics, even though it is not composed of chiral elements.

2.2. Experimental Results. The L-type PB coding metasurface has been fabricated, as shown in Figure 6a, and measured in an anechoic chamber, as shown in Figure 6b. A pair of CP horns are used for emitting and receiving the signals, in which the emitting horn and the metasurface are placed on a rotating platform with a distance about 60 cm to make sure that the incident waves are plane waves and normally illuminate the metasurface, while the receiving horn is placed in the other side of the anechoic chamber to receive the reflected signals, and the distance between the sample and receiver is about 9 m to satisfy the far-field measurement condition. It is worth mentioning that the emitting horn and receiving horn have the same polarization property, that is, the emitting signal and receiving signal have the same spin state. The measured far-field radiation patterns of LCP and RCP waves are demonstrated in Figure 6c,d, respectively, which are normalized to the reflection power generated by the bare copper plate with the same size. The results show that the LCP waves are efficiently reflected without reversing the polarization state, whose reflection angles are −31.9, −28.8, −24.5, −23.3, and −22.8° at 16, 18, 20, 22, and 24 GHz, respectively. While the RCP waves are randomly diffused, achieving a low RCS scattering in a broad frequency band from 16 to 24 GHz. The measured results are basically consistent very well with the simulation results shown in Figure 4b,c except for some slight deviation, which are mainly caused by the errors of fabrication and measurement. Figure 6e,f shows the simulated and measured reflection coefficients of the L-type PB coding metasurface, which are obtained by normalizing the reflection energy of the metasurface to that of a bare copper plate with the same size. The results show that the reflection efficiency of the main beam of LCP waves can be as high as 80% from 16 to 24 GHz, while the RCP waves are strongly suppressed with reflection coefficient less than 10%. The measured results show a good agreement with the simulations, validating that the proposed PB coding metasurface exhibits a broadband spin-selective reflection characteristic. In addition, the performance of the proposed PB coding metasurface compared to the existing works in terms of the bandwidth is illustrated in Table 1, which further shows that the proposed PB coding metasurface has an obvious advantage in a ultra-wide spin-selective frequency band, with relative bandwidth up to 30%.

| relative bandwidth | ref 19 single frequency@5.65 GHz | ref 20 single frequency@37.0 THz | ref 21 single frequency@9.00 GHz | ref 22 single frequency@9.50 GHz | ref 23 single frequency@0.60 THz | ref 24 dual frequencies@12.1 GHz and 14.4 GHz | ref 26 5.1% (9.89–10.41 GHz) | this work 30% (16–24 GHz) |

3. CONCLUSIONS

We propose a PB coding metasurface that is composed of spin-decoupled coding elements. By elaborately designing the coding phase distributions of the metasurface, the broadband spin-selective reflection with the arbitrary wavefront manipulation can be realized in the microwave regime. In addition, the results show that the PB coding metasurface also has the chiral-like characteristics, even though it is constructed by the nonchiral spin-decoupled elements, which is because the PB coding metasurface composed of these nonchiral spin-decoupled elements exhibits the characteristics of breaking both the \( n \)-fold (\( n > 2 \)) rotational and mirror symmetries. Both simulated and measured results validate the broadband characteristic of the proposed PB coding metasurface in the spin-selective wavefront manipulation. Compared with the conventional chiral metamirrors that are based on the asymmetric resonant structures, the proposed work opens up a new avenue for realizing the broadband spin-selective devices.

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