Book Chapter

Removal of Cadmium (II), Chromium (III), and Lead (II) Heavy Metal Ions from Water by Graft Copolymerization of Acrylonitrile onto Date Palm Fiber Using H$_2$O$_2$/Fe$^{++}$ as an Initiator

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Abstract

The study aims to assess how the date palm wood fibers (DPWF) can be used for the removal of heavy metals from water. The study involved examination of the radical polymerization and graft polymerization parameters such as reaction period, reaction time, monomer volume, amount of the catalyst, and concentration of initiator to obtain the maximum yield of graft polymerization. Fiber and copolymer were characterized using SEM and FT-IR spectroscopy to ensure the completion of polymerization. Hydroxylamine hydrochloride was used for treating the grafted copolymers for the preparation of polyamidoxime chelating resin, which was then examined for removing the heavy metal ions. Different resin dosages, contact
time, and initial concentrations were used, and the batch technique experiment was utilized. The study also applied the Langmuir and the Freundlich isotherm model, and Langmuir was found to be better. The absorption ability was found to be better for polyamidoxime resin for metal ions of cadmium (II), chromium (III), and lead (II).

**Keywords**

Cadmium (II); Chromium (III); Graft Copolymerization; Heavy Metal Ions; Lead (II)

**Introduction**

Discharge of heavy metals in the industrial effluents has increased the problem of water pollution [1]. Previous studies have revealed that non-biodegradable heavy metals tend to accumulate in the bodies of living organisms and for the same reason they are more hazardous as compared to other water pollutants [2]. Copper, silver, zinc, selenium, cadmium, mercury, lead, nickel, chromium, tin, iron, arsenic, gold, molybdenum, cobalt, manganese, aluminum, etc. are some commonly found heavy metals [3], which are proved to be harmful for humans and other living organisms [1]. Fu & Wang [4] stated that regular deposition of heavy metal subsequently causes severe damage to the central nervous system, skin, kidneys, teeth, liver, or lungs, and could also lead to death. Additionally, the removal of heavy metals is also challenging on account of their non-biodegradability [5].

In order to address this issue, researchers are focusing on the use of natural and bio-based materials [6]. Various kinds of biobased materials have been introduced, which may be based on cellular fibers, wood or protein and help in reducing the harmful effects caused by non-biodegradable elements [7]. Similarly, for the removal of heavy metals from aqueous solution, different methods, including precipitation and membrane processes: reverse osmosis, ion exchange, ultrafiltration, and more, are being used [8]. The use of precipitation after coagulation is limited on account of high sludge volume. Studies have
identified membrane filtration as a cost-effective way of ensuring the removal of metal ions; however, its cost is a major impediment in its implementation [9,10].

Kanamarlapudi, Chintalpudi, & Muddada [10] found absorption as an efficient, simple, and effective approach the removal of heavy metals from the wastewater; however, its high cost is also major challenge in its implementation. These challenges instigated scholars and researchers to find or develop cost-effective, eco-friendly, and non-conventional absorbents [9]. Recently, the interest in the use of plant-based fiber has increased, which are commercially in the production of polymer composites [1]. These composites can be used for removing the heavy metal ions from water especially when conventional methods are proved ineffective [11]. In order to satisfy and solve the above-mentioned problems, some natural materials such as cellulose, chitosan, chitin, and their derivatives have been specified as good and inexpensive options because of their economic efficiency, absorbent properties, safety, and biodegradability.

Ion exchange is a reaction in which free mobile ions of a solid are exchanged with different ions of identical charge in a solution. The exchanger contains an open network structure, either organic or inorganic, which carries the ions and let ions to pass through it. Ion exchangers may be organic or inorganic and are natural or synthetic materials such as synthetic resins which function as ion exchangers based on three-dimensional organic networks bearing charged or potentially charged groups [12]. Past research has shown increased interest in the use of date palm as a biodegradable material [13].

Recently many studies have focused on exploring an alternative metal adsorbent and grafted polymers. Grafting is the method in which functional monomers are covalently bonded to the backbone polymer chain [14-17]. Graft polymerization is significant as it permits implementing different functions of the grafted monomer on the parent polymer while retaining the mechanical features of the parent polymer. Radiation-induced grafting technique is dominant over all other approaches
implemented to initiate graft copolymerization such as ultraviolet light, decomposition of chemical initiators oxidation of polymers, plasma treatment, and ionizing radiation because of its extensive penetration into the polymer matrix and its rapid and homogeneous development of radicals [18, 19].

Date palm ("Phoenix dactylifera"), is abundantly grown throughout Saudi Arabia and its global production rate is 42%. It is an edible fruit with a papery skin, and a single, long, narrow, hard seed. There are many uses of date palm wood; for instance, it is used as posts and rafters for huts because it is lighter than coconut. It is also used in the construction of aqueducts, bridges, and parts of boats and dhowes. Moreover, the tree residues are used as fuel [20]. Date palm contains three major components: cellulose, lignin, hemicellulose, and other minor constituents such as protein and oil [21].

The focus of this is on date palm on account of its abundance, cost-effectiveness, and renewability in the Kingdom of Saudi Arabia. Its fiber produces biodegradable materials when treated with certain monomers and can be obtained at low costs in comparison with the costly plastic materials which are commonly used for removing metal ions from water. The limitations associated with heavy metals have led to extensive researches for the production of cost-effective alternatives which should be excessively available as waste materials. In the current study, the effectiveness of date palm fibers as low-cost bio-absorbent of heavy metals have been studies, with a focus on the impacts of the different reaction parameters that influence the adsorption efficiency.

**Modified Date Palm as Adsorbent of Heavy Metals**

In 30 countries, approximately 120 million date palm trees are cultivated covering an area of 800,000 hectors [22,23]. The investigation of the regional distribution shows that approximately 60 million date palm trees are located in Iran, Iraq, Oman, Pakistan, Saudi Arabia, Yemen, Bahrain, and Turkmenistan, and almost 32.5 million date palm trees are located in Africa. El-Hendawy [24] investigated the adsorption
capacities of date pit activated carbons with respect to Pb$^{2+}$ and Cd$^{2+}$. Data were compatible with the Langmuir model, which substantially contributed to the increase in adsorption capacity in comparison with raw date pits, and subsequently led to the increase in the adsorption of lead. The consumption was higher than cadmium due to its suitable pH for complexation or deposition and lower solubility. El Nemr et al. [25] assessed the removal of toxic chromium (VI) from different aqueous solutions with the help of an adsorbent containing activated carbon obtained date palm seed. The optimum pH for absorption was 1.0, and the increase in pH decreased the adsorption percentage. 120.48 mg/g was the maximum adsorption capacity for chromium (VI) and the equilibrium was obtained in 180 min due to the fast adsorption process. Studies have shown that the use of date stone and palm tree waste increases the Cu$^{2+}$ adsorption, where equilibrium was obtained within 120 min [26,27]. Hilal et al. [28] stated that maximum absorption capacity of activated date pits was at pH 5.8±0.5, which was five times greater than that of the raw date pits.

Abdulkarem & Al-Rub [29] studied the removal of lead (II) onto activated carbons, and 8-hydroxyquinoline modified activated carbons from date pits. The adsorption capacity was high in both the carbons; however, no significant improvement was found in adsorption after modification. Removal of Pb (II) ions using activated carbons was increased with an increase in pH. This process followed pseudo-second-order kinetics. Langmuir and Freundlich’s models showed good agreement from the equilibrium data for the adsorption of lead (II) ions. Yadav et al. [30] showed that date palm fibers can remove 99.955 chromate anions (Cr$^{6+}$) from a 100 mg L-1 solution with the use of a small absorbent dosage, i.e., 1.2g L-1.

Tunisian date stones activated via phosphoric acid were used for the removal of copper (II) from aqueous solutions. The best-activated carbon for the removal process was obtained with 60% phosphoric acid and an impregnation ratio of 1.75 at 450 °C. Dubinin-Kaganer–Radushkevich and Langmuir adsorption isotherm models were enough to explain the adsorption of copper (II) onto activated carbon. ($q_e$) which was found to be
31.25 mg/g. Bouhamed et al. [26] suggested a chemisorption process from kinetic data that were compatible with the pseudo-second-order kinetic model.

El-Shafey & Al-Kindy [31] modified leaflets of date palm using the sulphuric acid method at 170 °C. They suggested that the hot sulphuric acid dehydrates and induces reduction property in carbon. This carbon was used to remove copper and silver from aqueous solution using various parameters such as contact time, pH, temperature, and metal concentration. Adsorption of copper was greater as compared to the adsorption of silver as the equilibrium was reached within ~2 h and ~60 h respectively. The adsorption of copper was carried out through the diffusion-controlled ion exchange process; however, the value of activation energy of silver indicated chemisorption of silver ions into carbon.

The adsorption capacities of raw date pits and CO₂ activated date pits were compared with respect to the adsorption of copper and zinc ions. Banat et al. [32] found adsorption of both copper and zinc onto raw date pits higher than adsorption onto activated date pits carbon. This attributed to the difference in the surface functional groups of date pits and activated date pits. The heating during the activation process may have destroyed the functional groups that facilitate binding of zinc and copper. The removal of copper was better in comparison with the removal of zinc with respect to both the materials on account of its small ionic radius that facilitates an easy movement into porous surface. The best result was obtained at pH = 5 and temperature 25°C.

**Methodology**

**Materials and Reagents**

A non-woven polyethylene fabric was used as a trunk polymer for graft polymerization; the material was obtained from Kurashiki MFG Co. Monomer acrylonitrile (BDH, England) was used for grafting onto trunk polymer. Sodium carbonate, methanol, acetone, and sulphuric acid were obtained from Merck, Germany and hydroxyl amine hydrochloride was obtained from Sigma Aldrich, USA. Cadmium (II), lead (II)
acetate trihydrate (Merck, Germany), and chromium (III) (Techno pharmchem, India) were used for metal adsorption study. Date palm fibre was obtained from local market and the size of the fibre was less than 200 μm. The fibre was washed two times with hot distilled water and acetone. The acetone was removed by heating the fibre in an oven at 60 °C.

FTIR Spectroscopy

Infrared (IR) spectra of the DPW, grafted DPW, and the poly (amidoxime) ion-exchange resin samples were recorded on a Fourier transform–IR spectrometer (Perkin–Elmer 1725, Norwalk, CT) using a KBr disk pellet.

Scanning Electron Microscopy (SEM)

The SEM photographs of the fibre surfaces of grafted PAN onto DPW and ungrafted DPW fibre were captured using a scanning electron microscope model SEM JEOL 6400 (JEOL, Peabody, MA).

Preparation of a Chelating Resin containing Polyamidoxime Groups

Hydroxylamine hydrochloride (NH₂OH.HCl) solution was prepared by dissolving 20 g (0.288 mol) of hydroxylamine hydrochloride in 300 ml of a methanolic aqueous solution (methanol/water ratio = 80). The hydrochloride content of NH₂OH.HCl was neutralized by the addition of NaOH solution and the precipitated NaCl was removed by filtration. The grafted product was placed in a two-necked flask equipped with a condenser; the flask was placed in a thermostatic water bath and the hydroxylamine solution was poured in it. The mixture was allowed to react at 70°C with continuous stirring for 180 min. After completion of the reaction, the resin was filtered and washed several times with the methanolic solution. The resin was neutralized by treating it with 0.1 M HCl solution for 15 min; afterwards, it was again filtered, washed several times with the methanolic solution, and then dried in an oven at a constant weight at 60 °C.
Sorption of Lead Cadmium, and Chromium ions using the Batch Technique

The lead, cadmium, and chromium ions adsorption capacity of the resin were measured over the pH range 1–6. Thus, ca. 0.1 g of dried resin was placed in a series of 100 ml polyethylene bottles and equilibrated with 20 ml of distilled water. After adding 20 ml of 0.1 M sodium acetate buffer solution in each bottle, 10 ml of 0.1 M lead-ions solution was added. The resulting mixture was shaken for 24 h by a rotary shaker and afterwards, 5 ml of the supernatant was collected for the determination of metal-ions. AGBC-903 atomic absorption spectrometer was used to determine the initial and final amounts of metal ions present in the solutions.

Blank experiments were performed and the same experimental procedure was conducted for checking the adsorption level by the membrane filters and glass flasks for all adsorption tests. The kinetic samples were conducted in 1000 mL batch reactors at 20.0 in deionized water. The flasks were vigorously and magnetically stirred for 1.5 h for hydrating the beet pulp to naturally maintain the pH at 5.5.

Graft Copolymerization

To prepare the fibre/PAN copolymer, 1.00 g DPW fibre was placed in 250 ml three-necked flasks equipped with a stirrer and condenser, and immersed into a thermostatic water bath. The DPW suspension was obtained by adding 100 ml distilled water and 0.1g ferrous ammonium sulphate with continuous stirring. Nitrogen purged through the DPW fibre slurry to remove oxygen during the reaction. After 30 min, the required volume of 2.0M H₂O₂ was added and the mixture was mixed for 5 min; afterwards, the required amounts of monomer (AN) were added into the mixture. The reaction mixture was stirred under nitrogen at the chosen temperature and for the predetermined reaction period. Immediately after the reaction, the reaction flask was cooled by placing it under running tap water, and the product was filtered. The crude product was washed thoroughly with distilled water and oven-dried at 60°C at a constant weight.
Removal of Polyacrylonitrile and determination of Graft Level

The crude product was purified with N, N-dimethylformamide using a Soxhlet’s extractor for 48h to remove the polyacrylonitrile (PAN). The pure grafted copolymers were then dried at 65°C at a constant weight. The following formula determined the percentage of grafting (Pg).

\[
P_g = \frac{W_2 - W_1}{W_1} \times 100
\]  

(1)

Where \( W_1 \) is the weight of the original DPW fibres in grams, \( W_2 \) is the weight of the grafted product after copolymerization and extraction [33].

Graft Copolymerization

Date palm wood fiber (DPWF) was treated with mixed solution of hydrogen peroxide and ferrous ammonium sulfate to initiate a free radical in the backbone of the fiber and provide cellulose macro-radical. Graft copolymerization occurred after adding acrylonitrile (AN) monomer to the mixture during which the cellulose macro-radical broke the double bond in AN and a covalent bond between monomer and cellulose was formed, the chain initiated with continues creation of free radical on the AN. Chain grafting onto the cellulose was possible by adding AN monomer subsequently. The reaction was ultimately terminated either by the formation of a copolymer on account of the reaction of two macro-radical or formation of poly (methacrylate) by the reaction of two monomer radicals. Figure (1) explains the whole process [34,35].
Figure 1: Mechanism of graft copolymerization of Acrylonitrile onto DPWF.

**Optimization of Grafted Polymerization Parameters**

Effects of various parameters on the yield of grafted copolymerization were studied. These parameters included temperature, reaction time, monomer volume, co-catalyst amount and concentration of initiator. All these parameters were studied separately to investigate the best conditions and to obtain the best yield.
Effect of Temperature

A wide range of temperatures was used to obtain the best yield of the grafted copolymer. Figure (2) illustrates the effect of temperature that increase in temperature from 30 ºC up to 75 ºC increases the % yield of grafting. This increase could be attributed to the increase of monomer diffusion into the active sites on the backbone of the substrate. If temperature goes above 75 ºC, the monomer starts to evaporate, and hydrogen peroxide decomposes. This condition leads to creation of a huge number of free radicals, the yield of a homopolymer will increase and % of the grafted copolymer in pg will decrease [36, 37].

![Figure 2: Effect of reaction temperature on the % of grafting in pg. Reaction time 60 min, AN 8 ml, H₂O₂ 0.03 M, Fe⁺² 0.3 mmol, (Δ) % of grafting.](image)

Effect of the Concentration of Initiator

The yield of grafted polymer is clearly affected by the concentration of the initiator. As shown in Figure (3), the % of grafting increased with the increase in the concentration of the hydrogen peroxide as it increases the production of free radicals in the active sites of the fibre. At 0.03 M concentration, 81% grafting was obtained. However, the grafting percentage decreased with further increase in the percentage of hydrogen
peroxide because of the reaction between cellulose radicals before addition of monomers and this reaction is the termination step. Moreover, at higher concentrations, the yield of homopolymer increases [34].

**Figure 3:** Effect of the amount of initiator H$_2$O$_2$ on the % of grafting. Reaction time 60 min, AN 8 ml, Temperature 75 °C, Fe$^{2+}$ 0.3 mmol, (Δ) %of grafting.

**Effect of the Amount of Monomer**

The percentage of grafting increased with the increasing volume of the (AN) monomer on account of the availability of a large number of monomer molecules reaching the active sites in the backbone of the fibre. However, as shown in Figure (4), increase in volume over 8 ml decreased the percentage of grafting on account of the increased possibility of homopolymerization [37,38].
Figure 4: Effect of the amount of monomer (AN) on the % of grafting. Reaction time 60 min, H$_2$O$_2$ 0.03 M, Temperature 75 °C, Fe$^{2+}$ 0.3 mmol, (∆) % of grafting.

Effect of Reaction Period

The percentage of grafting was found directly proportional to the increase in the reaction time and it increase the time available to all monomer molecules to reach the active sites on the backbone; however, maximum grafting yield was obtained with the reaction time of 60 minutes. Afterwards, all active sites were covered, and the concentration of all reaction species decreased and this accounted for the low yield of grafting which almost remains constant with increasing time [39]. This explanation is in line with the results shown in Figure (5).

Figure 5: Effect of reaction period on the % of grafting and efficiency. AN 8 ml, H$_2$O$_2$ 0.03 M, Temperature 75 °C, Fe$^{2+}$ 0.3 mmol, (∆) % of grafting.
Effect of the Amount of Catalyst

Small amount of ammonium ferrous sulphate \([(NH_4)_2SO_4\cdot FeSO_4\cdot 6H_2O]\) was found to be enough for the best yield of a product (Figure 6), where 0.306 mmol of catalyst gave 81% of grafting product. This yield decreased with the increase in the amount of the catalyst on account of large number of radicals produced by the decomposition of hydrogen per oxide. The reaction finally terminates due to the reaction between radicals and yield will decrease [33,40].

![Figure 6: Effect of the amount of catalyst Fe²⁺ on the % of grafting. AN 8 ml, H₂O₂ 0.03 M, Temperature 75 °C, 60 min, (Δ) % of grafting.](image)

Preparation of Polyamidoxime Resin

The AN-DPWF grafted copolymer containing nitrile group was treated with hydroxylamine hydrochloride at pH 11 to change the nitrile group into amidoxime. This reaction was performed for 3 hours at 75°C, and the ratio between grafted copolymer and hydroxylamine in methanolic solution was 1:1. The mechanism of this conversion is shown in Figure (7).
Characterization of AN-DPWF Grafted Copolymer and Resin

FT-IR spectra were obtained for DPWF, grafted copolymer, and amidoxime resin to confirm the completion of polymerization and conversion of grafted copolymer into the chelating resin. In the Figure (8), same characteristic adsorption bands for DPWF, such as broad absorption band between 3000–3500 cm\(^{-1}\) was assigned to O-H stretching vibration and bands that appeared at 2900 and 1020 cm\(^{-1}\) for C-H stretching and bending modes, respectively. The characteristic adsorption at 2240 cm\(^{-1}\) for C≡N stretching modes confirm the presence of acrylonitrile onto the backbone of DPWF and grafting reaction completely [41].

This band was disappeared completely after conversion to amidoxime resin and new adsorption band formed at 1650 cm\(^{-1}\) associated with C=N vibration of amidoxime group. Another adsorption band observed at 941 cm\(^{-1}\) may be assigned to the N–O bond of the oxime group [42]. Scanning electron microscope (SEM) images were taken for DPWF before and after polymerization to investigate the changes in the morphology of the fibre surface. Figures (9) and (10) showed the surface of the fibre before and after grafted polymerization respectively. As can be seen in the Figure (10) all pours on the DPWF surface were covered with polyacrylonitrile (PAN) via the chemical bond and this covering yielded a homogeneous surface with less porosity.
Figure 8: FTIR DPWF fiber (—), AN-g-DPWF fiber (−−) and resin containing amidoxime groups (...).

Figure 9: Scanning electron micrographs of DPWF before grafting, SEM MAG. (1.36 KX).
Effect of initial pH

The pH solution is a substantial parameter used in the study of the removal of heavy metal ions from aqueous solution or water on account of many reasons such as its effects on the concentration of counter ions placed in adsorbent functional clusters, the level of ionization of the adsorbate during the reaction, and the solubility of metal ions. Batch technique was conducted to find out the optimum pH level required for the removal of heavy metals using amidoxime chelating resin. The concentration of the counter ions on the resin, ability of ionization and solubility of adsorbates depend on pH [43]. A wide range of pH (1.0 to 6.0) was investigated to get the optimum pH for a fixed concentration of metals and dosage of resin at 25 °C. The adsorption of lead (II), Cr (III) and Cd (II) was maximum at the pH=5.0 as shown in Figure (11). At low pH (< 3.0), the competition between H⁺ ions for the resin sites increased and the resin’s chelating ability was greatly reduced. At pH 5, the competition of H⁺ ions for the resin sites decreases and the chelating ability of the metal ion increases [44]. Equation (2) is used to calculate the percentage of the removal of metal ions using this resin [39,45,46].
\( \% \text{ of Removal} = \frac{C_0 - C_t}{C_0} \times 100 \)  \hspace{1cm} (2)

\textbf{Figure 11:} Effect of pH on the adsorption of (Pb^{2+}) (Cr^{3+}) and (Cd^{2+}) ions, dosage of chelating resin 1g ions concentration 50 mg/L, time 60 min, and temperature 25 °C.

\textbf{Effect of Contact Time and Initial Concentration}

The contact time is one of the important parameters to study as it affects the adsorption of heavy metals onto chelating resin. From Figure (12), it can be observed that the adsorption of heavy metals increases with increase in the contact time. Also, the adsorption was fast in the beginning until it reaches equilibrium at 35 min and, afterwards, the value of \( q_t \) (mg/g) remain constant. This can be attributed to the availability of active sites on the surface of chelating resin in the beginning of reaction \[47\]. Initial concentration of metals under study lead (II), Cr (III) and Cd (II) influenced the removal of these metals. The amount of metal ions, \( q_t \) (milligrams per gram) adsorbed is calculated by increasing the initial concentrations. Following equation is used to calculate metals ions adsorption at certain time, \( t \) (qt mg/g):

\[ q_t = (c_0 - c_t) \times \frac{V}{m} \]  \hspace{1cm} (3)
This can be illustrated by the ratio between available surface and initial metal ion concentration. On higher concentration, this ratio was low and it increased with the lower concentration and the initial concentration also affects the removal of heavy metals [48].
Figure 12: Effect of contact time on (A) lead (II), (B) Cr (III) and (C) Cd (II) adsorption at different initial feed concentration, solution pH 5, and temperature 25 °C.

Effect of Adsorbent Dosage

The efficiency of the amidoxime chelating resin dosage was investigated on the basis of its initial concentrations. Adsorption of lead (II), Cr (III), and Cd (II) was studied with different dosage of resin and 50 mg/L as initial concentration of metals at 25 °C and pH=5. According to Figure (13), when the resin dosage was increased from 0.05 g/L to 2g/L, the percentage of removal from 61.1% to 87.84% for Lead (II), from 49.94 to 71.50 % for chromium (III) and from 50.26 to 67.48 for cadmium (II) was observed. This increase in the removal percentage can be attributed to the availability of huge surface area and number of active sites on account of increase in the dosage of resin at constant concentration of metal ions.
Adsorption Kinetics

To investigate the adsorption mechanism and reaction pathways, some adsorption kinetic studies were conducted. Various kinetic models were applied to analyse the adsorption process of lead (II), Cr (III), and Cd (II) onto chelating resin. These models include pseudo first-order, pseudo-second-order, and intraparticle diffusion. Models with high correlation coefficients ($R^2$) may describe the adsorption of metal onto chelating resin.

The Pseudo-First-Order Model

The pseudo-first-order kinetic model illustrates the adsorption mechanisms in solid–liquid systems, which is generally expressed as:

$$\log(q_e - q_t) = \log q_e - \frac{k_1 t}{2.303}$$  \hspace{1cm} (4)

Where $k_1$ is the rate constant of pseudo-first-order adsorption (per minute) and $q_t$ and $q_e$ are the quantity of metal ions adsorbed (milligrams per gram) at time $t$, and equilibrium respectively [39, 49]. The plots of log ($q_e - q_t$) versus $t$ demonstrated in Figure (14), give the value rate constant $k_1$ and
adsorption density $q_e$ from the slope and intercept respectively. Bad linearity was obtained for this model and it was clear from the values of correlation coefficients ($R^2$) which was low for different concentrations. Moreover, no agreement was observed between the experimentally observed equilibrium adsorption ($q_e$, exp) and that derived theoretically ($q_e$, cal), which means that the adsorption of metal ions onto chelating resin kinetic data were not compatible with the pseudo-first-order kinetic model.
Figure 14: Lagergren first-order plot for adsorption of (A) Pb (II), (B) Cr (III), and (C) Cd (II) on amidoxime chelating resin for different initial feed concentration at pH 5 and temperature 25 °C.

The Pseudo-Second-Order Equation

The pseudo-second-order adsorption kinetic rate is expressed as:

$$\frac{dq_t}{dt} = k_2 (q_e - q_t)^2$$  \hspace{1cm} (5)

Where $k_2$ is the rate constant of the pseudo-second-order sorption (g/mg.min), $q_e$ and $q_t$ are the sorption capacity at equilibrium and time $t$ (mg/g) respectively. For the boundary conditions $t = 0$ to $t = t$ and $q_t = 0$ to $q_t = q_e$, the integrated form of Equation (5) will be as:

$$\frac{1}{q_e - q_t} = \frac{1}{q_e} + k_2 t$$  \hspace{1cm} (6)

Equation (6) can be expressed as:

$$\frac{t}{q_t} = \frac{1}{k_2 q_e^2} + \frac{t}{q_e}$$  \hspace{1cm} (7)

The initial adsorption rate, $h$ (milligrams per gram per minute) is given as:

$$h = k_2 q_e^2$$  \hspace{1cm} (8)
Equation 7 also can be written as:

\[
\frac{t}{q_t} = \frac{1}{h} + \frac{t}{q_e}
\]  

(9)

The plots of \(t/q_t\) versus \(t\) from Equation (9) at different concentrations of lead (II), Cr (III) and Cd (II) are shown in Figure (15). From slope and intercept, adsorption parameters \(q_e\) (Cal.) and \(k_2\) were calculated respectively (Table 1). The high linearity of the plots was indicated by values of correlation coefficients \((R^2)\) (≥ 0.99), which means that the adsorption kinetics between amidoxime chelating resin and heavy metals can be described using pseudo-second-order adsorption kinetic model. Moreover, the good agreement between \((q_e, \text{Cal.})\) and \((q_e, \text{Exp.})\) gives evidence for the compatibility of the adsorption data. This shows the adsorption of heavy metals onto amidoxime chelating resin occurs through chemical interaction between adsorbent and adsorbate [50-52].
Figure 15: Pseudo-second-order kinetic plot for adsorption of (A) Pb (II), (B) Cr (III), and (C) Cd (II) on amidoxime Chelating resin for different initial feed concentration at pH 5 and temperature 25 °C.

The Intraparticle diffusion Model

Adsorption mechanism and intra-particle diffusion rate determined steps of lead (II), Cr (III) and Cd (II) onto chelating resin was identified using Weber and Morris model. The rate constant for intra- particle \( (k_{id}) \) can be expressed as:

\[
q_t = k_{id} t^{1/2} + C \tag{10}
\]

Figure (16) shows the plots of \( q_t \) versus \( t^{1/2} \). It is clear that all lines for different concentrations do not pass through the point of
origin indicating the difficulty of predicting the mechanism of the overall process and it seems to be very complex [46, 53].

**Figure 16:** Intraparticle diffusion kinetic plot for adsorption of (A) Pb (II), (B) Cr (III), and (C) Cd (II) on amidoxime chelating resin for different initial feed concentration at pH 5 and temperature 25°C.
Table 1: Kinetic constant parameters obtained for heavy metal adsorption on polyamidoxime resin.

| Metal          | Pseudo-first order |                        | Pseudo-second order |                        | Intraparticle diffusion model |                        |
|---------------|--------------------|------------------------|---------------------|------------------------|-----------------------------|------------------------|
|               | C_i (mg/L)         | q_exp (mg/g)           | K_1 (10^-3) (min^-1) | q_cal (mg/g) | R^2 | K_2 (10^-2) (g/mgmin) | q_cal (mg/g) | h (g/min) | R^2 | K_id (mg/g/min) | C (mg/g) | R^2 |
| Lead (II)     |                    |                        |                     |                        |                             |                        |
| 70            | 22.40              | 41.22                  | 518.8               | 0.976                  | 0.30 | 17.95                  | 0.97         | 0.996     | 2.262 | 5.397           | 0.992     |
| 50            | 23.90              | 32.7                   | 226.01              | 0.976                  | 0.40 | 27.03                  | 2.91         | 0.992     | 1.733 | 10.521          | 0.990     |
| 30            | 13.81              | 53.19                  | 363.09              | 0.981                  | 0.24 | 27.85                  | 1.82         | 0.990     | 1.567 | 2.112           | 0.979     |
| Chromium (III)|                    |                        |                     |                        |                             |                        |
| 70            | 19.58              | 62.87                  | 1659.7              | 0.880                  | 0.08 | 32.79                  | 0.898        | 0.974     | 2.929 | 1.631           | 0.965     |
| 50            | 16.39              | 33.85                  | 111.88              | 0.994                  | 0.93 | 17.64                  | 2.89         | 0.995     | 0.856 | 9.645           | 0.986     |
| 30            | 10.72              | 29.48                  | 43.58               | 0.974                  | 0.31 | 14.47                  | 0.64         | 0.970     | 1.259 | 1.08            | 0.988     |
| Cadmium (II)  |                    |                        |                     |                        |                             |                        |
| 70            | 16.24              | 45.14                  | 832.6               | 0.937                  | 0.399 | 36.49                  | 0.53         | 0.947     | 2.745 | 3.999           | 0.983     |
| 50            | 15.54              | 53.19                  | 19.13               | 0.921                  | 1.1   | 16.86                  | 3.14         | 0.998     | 0.808 | 9.54            | 0.977     |
| 30            | 8.92               | 51.82                  | 72.31               | 0.924                  | 0.503 | 11.48                  | 0.66         | 0.986     | 0.977 | 1.662           | 0.967     |
Adsorption Isotherm Models

The adsorption efficiency of polyamidoxime chelating resin towards heavy metals was tested using some isotherm models. It describes the partition of adsorbate molecules between liquid and solid phase at equilibrium. Langmuir and Freundlich adsorption isotherm models were used to determine the adsorption capacity of amidoxime chelating resin towards lead (II), Cr (III) and Cd (II).

The Langmuir Isotherm Model

The Langmuir model assumes that the monolayer adsorption process takes place between adsorbate and adsorbent, and the surface is homogenous with finite number of active sites when sites are filled with adsorbate molecules. There is no chance of further adsorption on this site and saturation point is accomplished [54]. The linear equation is expressed as:

\[
\frac{C_e}{q_e} = \frac{1}{K_L q_m} + \frac{C_e}{q_m}
\]

(11)

Where \(C_e\) is the equilibrium concentration (mg/L) of metals in solution, \(q_e\) is the amount of metal ions adsorbed (mg/g) at equilibrium, \(K_L\) is Langmuir equilibrium constant (L/mg) and it is related to the affinity of adsorption sites and \(q_m\) gives the maximum theoretical monolayer adsorption capacity (mg/g). The values of \(q_m\) and \(K_L\) (Table 2) were obtained from slope and intercept respectively of plots of \(C_e/q_e\) versus \(C_e\), which are shown in Figure (17). The linearity and high values of correlation coefficients (\(R^2\)) indicate that the Langmuir model describes the adsorption process very well, confirming the formation of monolayer. Weber and Chakkravorti [55] defined the separation factor (\(R_L\)) as a characteristic dimensionless equilibrium parameter for Langmuir model and it is expressed as:

\[
R_L = \frac{1}{1+K_L C_o}
\]

(12)
The values of $R_L$ for each initial concentration was less than unity and greater than zero indicating the favourable adsorption of lead (II), Cr (III) and Cd (II) on poly amidoxime chelating resin [53].

**Figure 17**: Langmuir adsorption isotherms for adsorption of (A) Pb (II), (B) Cr (III), and (C) Cd (II) on amidoxime chelating resin, pH 5 and temperature 25 °C.
Table 2: Langmuir and Freundlich isotherm constants for Lead (II), Cr (III) and Cd (II) adsorption on amidoxime chelating resin.

| Compounds   | T (k)  | Langmuir isotherm constants | Freundlich isotherm constants |
|-------------|--------|-----------------------------|-------------------------------|
|             |        | \( q_m \) (mg/g) | \( K_L \) (L/mg) | \( R_L \) | \( R^2 \) | \( 1/n \) | \( n \) | \( K_F \) | \( R^2 \) |
| Lead (II)   | 298.16 | 43.86          | 9.12          | 0.002     | 0.999  | 0.04     | 23.15  | 48.62  | 0.8638 |
| Chromium (III) | 298.16 | 42.74          | 5.32          | 0.004     | 0.999  | 0.06     | 15.43  | 49.74  | 0.9701 |
| Cadmium (II) | 298.16 | 32.47          | 1.54          | 0.012     | 0.993  | 0.10     | 10.04  | 48.07  | 0.7647 |
Freundlich Isotherm Model

The Freundlich model is always used to describe the adsorption on heterogeneous surface of adsorbent [56]. Different initial concentrations of heavy metals were used with fixed dosage of amidoxime resin to obtain the equilibrium data. Freundlich isotherm model is expressed as follows:

\[ \ln q_e = \ln K_f + \frac{1}{n} \ln C_e \]  \hspace{1cm} (13)

Where \( K_f \) (mg/g) and \( n \) (g/L) are Freundlich adsorption constants. The plots of Lnqe against LnCe shown in Figure (18) give straight lines. From slope and intercept of those lines, the values of \( n \) and \( K_f \) can be calculated. Bad linearity and low values of correlation coefficient (R\(^2\)) indicate disagreement between equilibrium data and this model. Values of \( n \) more than unit mean favourable adsorption condition and lead (II), Cr (III) and Cd (II) are favourably adsorbed via amidoxime resin [53].
Figure 18: Freundlich adsorption isotherms for adsorption of (A) Pb (II), (B) Cr (III), and (C) Cd (II) on amidoxime chelating resin, pH 5 and temperature 25 °C.

Conclusion

This study used the grafted copolymerization of date palm wood fiber using hydrogen peroxide as initiator and ammonium ferrous sulphate as a catalyst. It studied the grafting parameters for obtaining the best grafting percentage. The grafting percentage depends upon the parameters such as the reaction period, reaction temperature, amount of the catalyst, concentration of the initiator and monomer volume. The best grafting percent was obtained using acrylonitrile monomer under following conditions: 8ml monomer, 0.03 M solution of hydrogen peroxide, and 0.306 mmol concentration of the catalyst. The reaction completed in 60 min at 75°C.
FTIR and STEM techniques were used for grafting products. Hydroxylamine was used for treating AN grafted copolymer for producing polyamidoxime chelating resins. The conversion process was confirmed using the FT-IR technique. Also, the batch template was used for examining the absorption capacity for heavy metal ions. The absorption pH value was found to range between 5 to 6. The better absorption behavior was observed for cadmium (II), chromium (III), and lead (II). The Langmuir isotherm found the correlation coefficient for resin to be 0.99, which was better than Freundlich isotherms.

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