Convective Heat Transfer of a Hybrid Nanofluid over a Nonlinearly Stretching Surface with Radiation Effect

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Abstract: The flow of the hybrid nanofluid (copper–titanium dioxide/water) over a nonlinearly stretching surface was studied with suction and radiation effect. The governing partial differential equations were then converted into non-linear ordinary differential equations by using proper similarity transformations. Therefore, these equations were solved by applying a numerical technique, namely Chebyshev pseudo spectral differentiation matrix. The results of the flow field, temperature distribution, reduced skin friction coefficient and reduced Nusselt number were deduced. It was found that the rising of the mass flux parameter slows down the velocity and, hence, decreases the temperature. Further, on enlarging the stretching parameter, the velocity and temperature increases and decreases, respectively. In addition, it was mentioned that the radiation parameter can effectively control the thermal boundary layer. Finally, the temperature decreases when the values of the temperature parameter increases.

Keywords: wall jet; hybrid nanofluid; radiation; surface temperature; numerical solution

1. Introduction

The analysis of flows due to stretched surface through heat transfer is considered, owing to their possible demands in several industrial procedures. The rate of stretching in a hot/cold fluids greatly depends upon the quality of the material with the desired properties. In such a process, heat transfer has an important role in controlling the cooling rate (see Fisher [1]; Tidmore and Klein [2]). Since the pioneer work done by Crane [3] on the boundary layer flow caused by stretching of elastic flat surface, a large number of researchers have investigated this problem from different points of view. The characteristics of flow and heat transfer in a boundary layer caused by a stretching/shrinking surface occurs frequently in many manufacturing processes in industry, including the extraction of polymer and rubber sheet, cooling of metallic plates, wire drawing, glassblowing, hot rolling and crystal growing, etc.

The topic of nanofluid is of scientific interest due to its many potential practical applications in biomedical, optical and electronic fields, etc. The mathematical nanofluid model was first developed by Choi [4] in 1995. Khanaf et al. [5], and Das and Tiwari [6] have examined the heat transfer performance of nanofluids inside an enclosure taking into account the solid particle dispersion. Later on, many authors discussed the effects of nanoparticles for different fluid models.

After Humenic and Huminic [7], these hybrid nanofluids are a species of fluids that contain extremely small particles of dimensions under 100 nm. They consist of two or three solid materials amalgamated with classical fluids (such as water, water ethylene glycol mixture or ethylene glycol, kerosene and engine, vegetable or paraffin oils). Many
particles can be used for the heat transfer enhancement of working fluids such as: Al$_2$O$_3$-Cu, Al$_2$O$_3$-Ag, Cu-TiO$_2$, Ag-TiO$_2$, Al$_2$O$_3$-SiO$_2$, etc. These fluids are utilized in tremendous heat transfer applications, such as heat pipes, micro-channel, mini channel heat sinks, plate heat exchangers, air conditioning systems, helical coil heat exchangers, etc. Comprehensive reviews on hybrid nanofluids were presented by Aly and Pop [8,9], Roșca et al. [10,11], Waini et al. [12,13], Devi and Devi [14], and in the review papers on hybrid nanofluids by Sarkarn et al. [15], Akilu et al. [16], Sidik et al. [17], Sundar et al. [18], etc.

Motivated by the above-mentioned studies, this paper considers the convective heat transfer of a hybrid nanofluid over a nonlinearly stretching surface with radiation effect. In addition, the problem statement is to be described in more detail in the next section. Further, the governing equations are converted into non-linear ordinary differential equations in Section 2. Moreover, Section 3 refers to the technique of the Chebyshev pseudospectral differentiation matrix that is applied to solve the resulted equations. The present results are plotted and then discussed in Section 4. To the authors’ knowledge, the present results are original and new.

2. Mathematical Model

Let us consider a hybrid Newtonian incompressible nanofluid over a flat stretching surface, where $x$ and $y$ are the Cartesian coordinates, which are assumed in such a manner that the $x$-axis runs along the surface and the $y$-axis is in the normal direction, the surface is laid down at $y = 0$, with the flow being at $y \geq 0$. The sheet stretches/shrinks with the velocity $u_w(x)$ and the surface temperature $T_w(x)$, while the constant ambient temperature is $T_\infty$. The mass flux velocity is $v = v_w(x)$ with $v(x) < 0$ for suction, while $v_w(x) > 0$ for injection, respectively, and the radiation term is $q_r$. The governing equations are subject to the assumption of slender boundary layer, which holds true for the case of a high Reynolds number. Under these assumptions, the governing conservation equations of mass, momentum and energy can be expressed in Cartesian coordinates $(x, y)$ (see Kazemi et al. [19] and Devi and Devi [20]):

\[
\frac{\partial u}{\partial x} + \frac{\partial v}{\partial y} = 0, \tag{1}
\]

\[
\frac{\partial u}{\partial x} + v \frac{\partial u}{\partial y} = \frac{\mu_{hnf}}{\rho_{hnf}} \frac{\partial^2 u}{\partial y^2}, \tag{2}
\]

\[
\frac{\partial T}{\partial x} + v \frac{\partial T}{\partial y} = \frac{k_{hnf}}{(\rho C_p)_{hnf}} \frac{\partial^2 T}{\partial y^2} - \frac{1}{(\rho C_p)_{hnf}} \frac{\partial q_r}{\partial y}, \tag{3}
\]

subject to the following boundary conditions:

\[
v = v_w(x), \quad u = \left[ u_w(x) = \frac{v_f}{L^{4/3}} x^{1/3} \right] \lambda, \quad T = T_w(x) + T_0 \left( \frac{x}{L} \right)^m \text{ at } y = 0, \tag{4}
\]

\[
u \to 0, \quad T \to T_\infty \text{ at } y \to \infty. \tag{5}
\]

where $u$ and $v$ are the velocity components along the $x$- and $y$-axes, $T$ is the fluid temperature of the hybrid nanofluid, $T_0$ is the characteristic temperature of the hybrid nanofluid, $L$ is the characteristic length of the surface taken as the streamwise surface extent, $q_r$ is the radiative heat flux, $m$ describes the nonlinear boundary condition for surface temperature, where $m \neq 0$ and $m \neq 1$, and $\lambda$ is the constant stretching parameter with $\lambda > 0$ and $\lambda = 0$ for stretching and static, respectively. In addition, the subscript $hnf$ refers the hybrid nanofluid quantities, where $\mu_{hnf}$ is the effective dynamic viscosity, $\rho_{hnf}$ is the effective density, $k_{hnf}$ is the thermal conductivity, and $(\rho C_p)_{hnf}$ is the heat capacitance, where $C_p$ is the specific heat at constant pressure. Further, the hybrid nanofluid quantities of Cu-Al$_2$O$_3$/water are defined as follows [20]:
\[
\frac{\rho_{\text{hf}}}{\rho_f} = (1 - \phi_2) \left[ 1 - \phi_1 + \phi_1 \frac{\rho_1}{\rho_f} \right] + \phi_2 \frac{\rho_2}{\rho_f}, \tag{6}
\]
\[
\frac{\mu_{\text{hf}}}{\mu_f} = \frac{1}{(1 - \phi_1) \sqrt[3]{(1 - \phi_2)^2}}, \tag{7}
\]
\[
\frac{(\rho C_p)_{\text{hf}}}{(\rho C_p)_f} = (1 - \phi_2) \left[ 1 - \phi_1 + \phi_1 \frac{(\rho C_p)_1}{(\rho C_p)_f} \right] + \phi_2 \frac{(\rho C_p)_2}{(\rho C_p)_f}, \tag{8}
\]
\[
\frac{k_{\text{hf}}}{k_f} = \frac{k_2 + 2k_{bf} + 2\phi_2 (k_2 - k_f)}{k_2 + 2k_{bf} - \phi_2 (k_2 - k_f)}, \quad \text{where} \tag{9}
\]
\[
k_{bf} = \frac{k_1 + 2k_f + 2\phi_1 (k_1 - k_f)}{k_1 + 2k_f - \phi_1 (k_1 - k_f)}.
\]

These correlations are based on physical assumptions and are in agreement with the conservation of mass and energy. Here, \(\phi_1\) and \(\phi_2\) are the hybrid nanoparticle volume fractions for \(\text{Al}_2\text{O}_3\) and \(\text{Cu}\), respectively, where \(\phi_1 = \phi_2 = 0\) correspond to a regular fluid. Further, the subscripts \((\_w, (\_t, (\_2\) and \((\_f\) refer to the wall, physical quantities of \(\text{Al}_2\text{O}_3\), \(\text{Cu}\) and fluid (water), respectively, as given in Table 1.

| Physical Properties | Base Fluid | \(\text{Al}_2\text{O}_3\) | \(\text{Cu}\) |
|---------------------|------------|----------------|--------|
| \(\rho\) (kg m\(^{-3}\)) | 997.1      | 3970           | 8933   |
| \(C_p\) (J kg\(^{-1}\) K\(^{-1}\)) | 4179       | 765            | 385    |
| \(k\) (W m\(^{-1}\) K\(^{-1}\)) | 0.613      | 40             | 401    |

Regarding the approximation of Rosseland for radiation, the radiative heat flux is simplified as follows (see [21,22]):

\[
q_r = -\frac{4\sigma^*}{3k^*} \frac{\partial T^4}{\partial y}, \tag{10}
\]

where \(\sigma^*\) is the Stefan–Boltzmann constant and \(k^*\) is the mean absorption coefficient. Now, by expanding \(T^4\) using a Taylor series about \(T_\infty\) and neglecting higher-order terms, \(T^4\) is expanded about \(T_\infty\) to obtain \(T^4 \approx 4T_\infty^3 - 3T_\infty^4\). By substituting the last expression in Equation (10) and then in Equation (3), the energy equation takes the following form:

\[
\frac{u}{\kappa} \frac{\partial T}{\partial x} + \frac{v}{\kappa} \frac{\partial T}{\partial y} = \frac{1}{\left(\rho C_p\right)_{\text{hf}}} \left( k_{\text{hf}} + \frac{16\sigma^* T_\infty^3}{3k^*} \right) \frac{\partial^2 T}{\partial y^2}. \tag{11}
\]

According to Kazemi et al. [19], we introduce the following dimensionless variables:

\[
u = \frac{v_f}{L^{4/3} x^{1/3}} f'(\eta), \quad \theta(\eta) = \frac{T - T_\infty}{T_\infty - T_\infty}, \quad \eta = \frac{y}{L^{2/3}}. \tag{12}
\]

Thus,

\[
v_w = \frac{1}{3} \frac{v_f}{L^{4/3} x^{1/3}} S_r, \tag{13}
\]

where prime denotes differentiation with respect to \(\eta\), and \(S\) is the constant mass flux parameter with \(S > 0\) for suction and injection flow, respectively, substituting...
the similarity variables (12) into Equations (2) and (11), it is found that they are reduced to the following ordinary (similarity) differential equations:

\[
3 \frac{u_{nf}}{u_f} f''' + 2 f'' - f'^2 = 0, 
\]

and the boundary conditions (4) become the following:

\[
f(0) = S, \quad f'(0) = \lambda, \quad \theta(0) = 1, \quad f'(\eta) \to 0, \quad \theta(\eta) \to 0 \quad \text{as} \quad \eta \to \infty, 
\]

where \( Pr = (\rho_C)_f/k_f \) is the Prandtl number and \( R = 4\sigma^4 T_0^4/k^4 k_f \) is the radiation parameter. The physical quantities of interest are the skin friction coefficient \( C_f \) and the local Nusselt number \( Nu_x \), which are defined as follows:

\[
C_f = \frac{\mu_{nf}}{\rho_{nf} u_w^2} \left( \frac{\partial u}{\partial y} \right)_{y=0}, \quad Nu_x = -\frac{x k_{nf}}{k_f (T_w - T_0)} \left( \frac{\partial T}{\partial y} \right)_{y=0} + x(q_r)_{y=0}. 
\]

Using Equations (12) and (18) results in the following:

\[
Sr = Re_x^{1/2} C_f = \frac{u_{nf}}{u_f} f''(0), \quad \text{Nur} = Re_x^{1/2} Nu_x = -\left( \frac{k_{nf}}{k_f} + 4 R \right) \theta'(0),
\]

where \( Re_x = u_w(x) x / \nu_f \) is the local Reynolds number, and \( Sr \) and \( Nur \) are the reduced skin friction coefficient and reduced Nusselt number, respectively.

3. Numerical Approach

The numerical technique of the Chebyshev pseudospectral differentiation matrix (ChPDM) is applied to solve Equations (14) and (15) subject to the boundary conditions (16). The works of Aly et al. [23], Guedda et al. [24], Aly and Vajravelu [25], Aly and Sayed [26], Aly and Pop [27] contain more details about this approach. In particular, one supposes that the problem’s domain is \([0, \eta_\infty]\), where \( \eta_\infty \) is the boundary–layer edge. Then, the following mapping

\[
\gamma = \frac{2 \eta}{\eta_\infty} - 1
\]

transfers the investigated domain to \([-1, 1]\) (the Chebyshev one). It should be noted that, in this interval, the associated collocation points are given by the following:

\[
\gamma_j = \cos \left( \frac{\pi}{N} j \right), \quad j = 0, 1, \ldots, N.
\]

Hence, the kth derivative of any function, say \( F(\gamma) \), at these collocation points is approximated as the following:

\[
F^{(k)} = D^{(k)} F,
\]

where \( D^{(k)} \) is the Chebyshev pseudospectral approximation of \( F^{(k)} \) and \( F = [F(\gamma_0), F(\gamma_1), \ldots, F(\gamma_N)]^T \) with \( F^{(k)} = [F^{(k)}(\gamma_0), F^{(k)}(\gamma_1), \ldots, F^{(k)}(\gamma_N)]^T \). Further, the entries of the matrix \( D^{(k)} \) are given by the following:

\[
d^{(k)}_{i,j} = \frac{2 \Omega_i}{N} \sum_{r=k}^{N} \sum_{t=0}^{r-k} \Omega_r \Omega_t (-1)^{r+t+k} \gamma_{i+j}^{(k)} \gamma_{i-j}^{(k)} \gamma_{|i-n|}^{(k)} \gamma_{|i-n|}^{(k)}.
\]
Here, \( \Omega_j = 1 \), except for \( \Omega_0 = \Omega_N = \frac{1}{2} \) and

\[
p^k_{\ell,r} = \frac{2^k r}{(k - 1)! c_\ell} \frac{(\chi - \ell + k - 1)! (\chi + k - 1)!}{(\chi)! (\chi - \ell)!},
\]

where \( 2\chi = r + \ell - k \) and \( c_0 = 2, c_j = 1, j \geq 1 \). Therefore, on applying the ChPDM approach, derivatives of the functions \( f(\gamma) \) and \( \theta(\gamma) \) at the points \( \gamma_i \) are taken as follows:

\[
f^{(k)}(\gamma_j) = \sum_{j=0}^{N} d_{ij}^{(k)} f(\gamma_j), \quad \theta^{(k)}(\gamma_j) = \sum_{j=0}^{N} d_{ij}^{(k)} \theta(\gamma_j), \quad k = 1, 2, 3, \quad i = 1, 2, \ldots, N.
\]

Therefore, Equations (14)–(16) become the following:

\[
3 \frac{\mu_{\text{nf}} / \mu_f \sum_{j=0}^{N} d_{ij}^{(3)} f(\gamma_j)}{\rho_{\text{nf}} / \rho_f} + \frac{\eta_{\text{nf}}}{2} \left( 2 f(\gamma_j) \sum_{j=0}^{N} d_{ij}^{(2)} f(\gamma_j) - \left( \sum_{j=0}^{N} d_{ij}^{(1)} f(\gamma_j) \right)^2 \right) = 0,
\]

\[
3 \left( \frac{k_{\text{nf}}}{k_f} + \frac{4}{3} R \right) \frac{\sum_{j=0}^{N} d_{ij}^{(2)} \theta(\gamma_j)}{Pr (\rho C_p)_{\text{nf}} / (\rho C_p) f} + \frac{\eta_{\text{nf}}}{2} \left( 2 f(\gamma_j) \sum_{j=0}^{N} d_{ij}^{(2)} \theta(\gamma_j) - \left( \sum_{j=0}^{N} d_{ij}^{(1)} f(\gamma_j) \right) \right) = 0,
\]

\[
 f(\gamma_N) = S, \quad \sum_{j=0}^{N} d_{Nj}^{(1)} f(z_j) = \frac{\eta_{\text{nf}}}{2}, \quad \theta(\gamma_N) = 1,
\]

\[
 \sum_{j=0}^{N} d_{0j}^{(1)} f(\gamma_j) = 0, \quad \theta(\gamma_0) = 0,
\]

Finally, it should be mentioned that the resulting nonlinear Equations (26) and (27) with the boundary conditions (28) contain \( 2N - 1 \) equations for the unknowns \( f(\gamma_j), \theta(\gamma_j), j = 1, 2, \ldots, N \) and \( \theta(\gamma_j), j = 1, 2, \ldots, N - 1 \). These equations are solved using the Newton method by executing them in MATHEMATICA \( g^{\text{TM}} \) software and running on a PC.

### 4. Results and Discussion

In this research, the Prandtl number \( Pr \) of the base fluid (water) is fixed at 6.2. Firstly, the nanofluid \( \text{Al}_2\text{O}_3/\text{H}_2\text{O} \) is produced by adding the \( \text{Al}_2\text{O}_3 \) nanoparticles with a fixed volume fraction \( \phi_{\text{Al}_2\text{O}_3} = 0.1 \). Then, the hybrid nanofluid \( \text{Cu-Al}_2\text{O}_3/\text{water} \) is made by mixing Cu-nanoparticles with \( 0 < \phi_{\text{Cu}} \leq 0.1 \) to this nanofluid. Influences of the various physical parameters on the velocity and temperature for the resulted hybrid nanofluid are presented in the remaining of the current section.

Impacts of \( S \) on the velocity profiles \( f'(\eta) \) and temperature distributions \( \theta(\eta) \) are presented in Figures 1 and 2, respectively. It can be seen from Figure 1 that the rising of \( S \) leads to slowing down the \( \text{Cu-Al}_2\text{O}_3/\text{water} \) velocity. This leads to decreasing the hybrid nanofluid temperature, as seen in Figure 2. Effects of the sheet parameter \( \lambda \) on \( f'(\eta) \) and \( \theta(\eta) \) are illustrated in Figures 3 and 4, respectively. As shown in these figures, as \( \lambda \) enlarges, the velocity and temperature increases and decreases, respectively.

Figure 5 presents the temperature distributions \( \theta(\eta) \) for various values of the thermal radiation (\( R \)). This figure shows that enlarging \( R \) increases \( \theta(\eta) \). It is known that the radiation parameter measures the relation between the conduction heat transfer and thermal radiation transfer. Hence, the increasing of \( R \) is indicative of a larger amount of radiative heat energy being poured into the system, which causes a rise in the temperature. Regarding this, the radiation can control the thermal boundary layers.
**Figure 1.** Velocity profiles $f'(\eta)$ for various values of $S$.

**Figure 2.** Temperature distributions of the hybrid nanofluid for various values of $S$.

**Figure 3.** Velocity profiles $f'(\eta)$ for various values of $\lambda$. 

Note: The figures show velocity profiles for various values of $S$ and $\lambda$, with specified parameters for $\phi_1$, $\phi_2$, $R$, $m$, and $\lambda$. The graphs illustrate the behavior of the velocity profile as $S$ and $\lambda$ change, with the velocity increasing or decreasing as appropriate.
Figure 4. Effects of $\lambda$ on the temperature distributions of the hybrid nanofluid.

Figure 5. Influence of the thermal radiation parameter $R$ on the temperature distributions.

Figure 6 indicates that an increase in the surface temperature parameter $m$ decreases the dimensionless temperature. Influences of the solid volume fraction $\phi_2$ on the temperature distributions are plotted in Figure 7. As seen in this figure, $\theta(\eta)$ increases as the Cu-nanoparticles concentration increases. This is because the rising of the hybrid nanofluid concentration generates more kinetic energy in the system. This means that $\phi_2$ plays an important role in the variation of the temperature. Effects of the reduced Nusselt number (Nur) as a function of $\eta$ for various values of $R$, $m$, $S$ and $\lambda$ are shown in Figure 8. From these figures, it can be seen that Nur increases by enlarging all of these parameters. The future research trends of this work may be stated as including the magnetic field strength, velocity slip parameters, effects of another hybrid nanofluid and variation of the radiation parameter.
Figure 6. Impact of $m$ on the temperature distributions of the hybrid nanofluid.

Figure 7. Impact of the Cu-nanoparticle volume fraction ($\phi_2$) on the temperature distributions.

Figure 8. Cont.
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5. Conclusions

In this research, the hybrid Newtonian incompressible nanofluid flow (Cu-Al$_2$O$_3$/water) over a nonlinearly stretching surface was investigated. Then, the governing equations were converted into non-linear ordinary differential equations by applying the proper similarity transformations. Hence, the resulted equations were solved, using the numerical technique Chebyshev pseudo spectral differentiation matrix.

It was deduced that the rising of the mass flux parameter $S$ slows down the velocity and, therefore, decreases the temperature. In addition, the velocity and temperature increases and decreases, respectively, when the stretching parameter $\lambda$ enlarges. Moreover, the temperature decreases when the values of the temperature parameter $m$ increases. Further, to control the thermal of hybrid nanofluid boundary layer, the radiation parameter can be effectively applied. Furthermore, the solid volume fractions of the included nanoparticle play an important role in the temperature distributions. Finally, the reduced Nusselt number (Nur) increases by raising the values of $R$, $m$, $S$ and $\lambda$.

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