Tidal waves in $^{102}$Pd: A phenomenological analysis

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Rotational and electromagnetic properties of the yrast band in $^{102}$Pd are analyzed in terms of a phenomenological phonon model that includes anharmonic terms. Both the moment of inertia and $B(E2)$'s are well reproduced by the model, providing an independent confirmation of the multiphonon picture recently proposed. The (empirical) dependence of the phonon-phonon interaction on the phonon frequency, in Ru, Pd, and Ru isotopes, follows the expectations from particle-vibration coupling.

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The subject of collective vibrational motion in nuclei has been a central theme of study in nuclear physics [1]. In particular, the existence of rather pure multiphonon states is still the subject of debate as the mixing with a background of quasiparticle states fragments the collective levels [2]. In a recent work [3], the yrast states of spherical or weakly deformed nuclei have been described as arising from the rotation-induced condensation of aligned quadrupole phonons. Semiclassically, this condensate represents running waves on the nuclear surface (tidal waves).

Recently, $B(E2)$ reduced transition probabilities in the yrast band of the nucleus $^{102}$Pd were extracted from lifetime measurements using the DSAM technique [4]. This new information, together with the level energies, was interpreted as evidence for tidal waves, and calculations based on the microscopic model of Ref. [3] account rather well for the observed properties. If the multiphonon picture of the yrast band in $^{102}$Pd is indeed valid, it should also be possible to explain its properties from the (complementary) point of view of a standard phonon model that takes into account anharmonic effects [1,5–8]. In this Brief Report, we present a phenomenological analysis based on such an approach.

In the simplest approximation of pure harmonic motion, the energy $E_n$ and the angular momenta $I$ of the yrast states are simply related to the number of phonons $n$ (of energy $\hbar \omega_0$) by

$$ E_n = n \hbar \omega_0 $$

and

$$ I = 2n $$

since each quadrupole phonon carries two units of angular momentum.

Considering the effects of anharmonic terms arising from the interaction between phonons [1,5,7,8], Eq. (1) gets modified as follows:

$$ E_n \approx n \hbar \omega_0 + \frac{1}{2} V_2 n(n - 1) + \frac{1}{6} V_3 n(n - 1)(n - 2) + \cdots $$

(3)

The good agreement with the data and the values of the coefficients indicate the applicability of the anharmonic expansion. This suggests the possibility of going one step further and studying the correlation between $\hbar \omega_0$ and $V_2$, obtained from the coefficients $a, b,$ and $c$ above. General arguments (see the discussions on p. 338 of Ref. [1]), indicate that as fluctuations of the spherical shape become increasingly pronounced the nucleus will eventually deform, and in the process of this shape transition the vibrations will be subject to large anharmonicities. Thus, we would expect that the more collective the phonon the larger the anharmonic terms, or in other words, $V_2$ to increase when $\hbar \omega_0$ decreases.

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1The reader may want to compare these results with those of Figs. 4 and 5 in Ref. [4].

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The theory of particle-vibration coupling [1,9–11] provides the tools to calculate the phonon-phonon interaction $V_2$ in terms of the microscopic properties of the basic phonons. In fact, the cases discussed in [9,10] (based on the Lipkin model [12]), confirm our qualitative expectation and predict for example:

$$V_2 \approx A - B\hbar\omega_0$$

for the exact solution, and

$$V_2 \approx \frac{C}{(\hbar\omega_0)^2}$$

in the perturbative approach.

We have extended the analysis of moments of inertia described above for $^{102}$Pd to neighboring Ru, Pd, and Cd isotopes and obtained the systematics shown in Fig. 2. As we have argued, $V_2$ displays a decreasing trend with $\hbar\omega_0$ which is compared to the expressions discussed above. While the overall behavior is reproduced, it would be of interest to see if the particle-vibration coupling approach, along the lines of the more realistic development in [11], can also account for the absolute scales. This could be the subject of a future study.

In summary, we have analyzed the properties of the yrast band in $^{102}$Pd on the basis of a phenomenological phonon model, that includes anharmonic terms. Both the moment of inertia and electromagnetic properties are well reproduced by Eqs. (5) and (6), and provide a complementary confirmation of the multi-phonon picture proposed in [3,4]. The relation between $V_2$ and $\hbar\omega_0$ in Ru, Pd, and Cd nuclei appears to be accounted for by the expectations from particle-vibration coupling.

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