The structure of the jet in 3C 15 from multiband polarimetry

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ABSTRACT

We investigate the structure of the kpc-scale jet in the nearby \((z = 0.073)\) radio galaxy 3C 15, using new optical Hubble Space Telescope (HST) ACS/F606W polarimetry together with archival multiband HST imaging, Chandra X-ray data and 8.4-GHz VLA radio polarimetry. The new data confirm that synchrotron radiation dominates in the optical. With matched beams, the jet is generally narrower in the optical than in the radio, suggesting a stratified flow. We examine a simple two-component model comprising a highly relativistic spine and lower-velocity sheath. This configuration is broadly consistent with polarization angle differences seen in the optical and radio data. The base of the jet is relatively brighter in the ultraviolet and X-ray than at lower energies, and the radio and optical polarization angles vary significantly as the jet brightens downstream. Further out, the X-ray intensity rises again and the apparent magnetic field becomes simpler, indicating a strong shock. Modelling the synchrotron spectrum of this brightest X-ray knot provides an estimate of its minimum internal pressure, and a comparison with the thermal pressure from X-ray emitting gas shows that the knot is overpressured and likely to be a temporary, expanding feature.

Key words: magnetic fields – polarization – galaxies: active – galaxies: individual: 3C 15 – galaxies: jets.

1 INTRODUCTION

The jets and lobes of radio galaxies are sites of some of the most energetic particles in the Universe. Many nearby sources show complex structures at all angular sizes, and most have been observed to emit synchrotron radiation from X-ray to radio wavelengths in their resolved jets. Much of the physics of these jets is unclear, although it is generally believed that they are relativistic, collimated outflows of plasma, launched from an active galactic nucleus by some largely unknown mechanism. The plasma contains magnetic fields that play significant roles in shaping the jets and producing the radiation we detect.

Early radio observations of kpc-scale jets revealed that the emissions were of synchrotron origin and often highly polarized, implying ordered magnetic fields within the jet (e.g. Bridle & Perley 1984). More recent observations have revealed optical counterparts to some radio jets, often showing a close correspondence in radio and optical morphology. Combined with optical spectra, this suggested that the optical emission was also synchrotron in nature (e.g. Keel 1988; Fedorenko & Courvoisier 1996, and references therein). The kpc-scale jets of most nearby radio galaxies observed with the Chandra X-ray Observatory (CXO) are detected in X-rays, and it has been argued that the dominant emission process is synchrotron radiation (Hardcastle, Birkinshaw & Worrall 2001; Worrall, Birkinshaw & Hardcastle 2001). Since the lifetime of high-energy electrons to synchrotron–radiation losses is short (tens to hundreds of years for electrons with \(\gamma = E/mc^2 \sim 10^7 - 10^8\) in a magnetic field of a few nT), it is clear that there must be significant localized particle acceleration occurring throughout the jet to maintain the observed emissions.

Magnetic-field structures are indicated primarily by the polarization pattern of the synchrotron radiation: polarization vectors show the direction of the apparent magnetic field, while the fraction of polarized emission indicates the ordering of the field. Multiband imaging and polarimetry therefore tell us about the magnetic fields seen by emitting particles of different energies.

3C 15 is a bright, compact and relatively nearby radio galaxy at redshift \(z = 0.073\), and it has an elliptical host galaxy showing weak optical emission lines (Tadhunter et al. 1993). At 8.4 GHz it is dominated by a luminous, one-sided jet, although it also exhibits diffuse emission from extended radio lobes and a weak counter-jet (Leahy et al. 1997, and fig. 1). The bright core is not resolved with the VLA. The radio morphology of 3C 15 is unusual: the northern jet is knotty and appears similar to those in Fanaroff–Riley (FR) class I sources, while the southern jet is barely detected in the radio. However, it powers a ‘warm spot’ in the southern radio lobe which is typical of a more powerful FR class II galaxy. The radio power of

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3C 15 (L_{178 MHz} = 3.3 \times 10^{25} \text{ W Hz}^{-1} \text{ sr}^{-1}, \text{from Hardcastle et al. 1999b}) is close to the FR I/FR II boundary at 10^{25} \text{ W Hz}^{-1} \text{ sr}^{-1} (Ledlow & Owen 1992).

An optical jet in 3C 15, closely following the morphology of the northern radio jet, was detected with the Hubble Space Telescope, and it has been suggested that synchrotron radiation dominates in both the radio and optical wavebands (Martel et al. 1998). The radio–optical spectral index of the integrated jet emission α_{opt} = 0.95 \pm 0.01 was the softest known at that time. The jet and lobes are detected in X-rays with the subarcsecond resolution offered by Chandra. Kataoka et al. (2003) presented four different models of the spectral energy distribution (SED) at the brightest X-ray knot in the jet; they favour a broad-band synchrotron spectrum with an equipartition magnetic field, and a cooling break at a Lorentz factor γ_{brk} = 2.6 \times 10^4. We agree with the general characteristics of this model, although the updated calibration products released by the Chandra X-ray Center (CXC) allow us to extract a more reliable X-ray spectrum of this region of the jet, and hence model the spectrum of the knot with greater confidence. Multiband optical photometry also allows us to place a good constraint on the optical spectral index α_{opt} in the knot.

In this paper, we re-examine the 3C 15 jet, using new HST optical polarimetry in conjunction with the reprocessed radio and X-ray data. Section 2 describes the multiwaveband observations we used. We present our results in Section 3, and in Section 4 we examine simple models of the jet and its flow. Detailed magnetic modelling of the jet is deferred to a later paper. Our primary aim is to use the apparent magnetic-field structure to infer characteristics of the plasma flow and locate sites of particle acceleration. Throughout, we adopt values for the cosmological parameters h_0 = 70 \text{ km s}^{-1} \text{ Mpc}^{-1}, \Omega_{\Lambda} = 0.7 \text{ and } \Omega_m = 0.3. \text{At the redshift of 3C 15, 1 arcsec corresponds to a projected distance of 1.39 kpc.}

2 OBSERVATIONS

2.1 Radio data

Archival X-band (8.4 GHz) VLA data of 3C 15 were reprocessed using the AIPS package from NRAO. We used data from a 20 min observation in the C-configuration on 1990 September 14, and those from an additional 87 min A-configuration (high-resolution) observation on 1990 May 26.

The data were read into AIPS and bad scans were flagged and removed. Antennas 26 and 29 were not present for the observation made using the A-array, while antennas 15 and 23 were removed due to high noise across all baselines. In the C-configuration, antennas 11, 23 and 29 were absent and antennas 6, 18 and 22 required further flagging. The first ten seconds of all scans were also removed to avoid problems with bad visibilities. Flux–density calibration used 3C 286 for the A-configuration data and 3C 48 for the C-configuration data, while both observations made use of 0040-017 as the calibrator source, both data sets were phase and amplitude aligned using the task CALIB in AIPS. The A- and C-array data were then combined using the method described by Black et al. (1992), and a further self-calibration was performed on the new data base. The large-scale intensity map was deconvolved using the maximum entropy method (MEM) embodied in the AIPS task VTESS, since it handles extended structure well. However, as pointed out by Black et al. (1992), MEM algorithms do not give good results near bright, compact regions. For the extended structure, we employ their hybrid technique of an initial shallow Clean, followed by 50 iterations of VTESS applied only to the residuals. The convolved Clean components were then restored to the VTESS image to give the Stokes I map (Fig. 1).

The radio emission from the jet was also imaged at the highest angular resolution in Stokes I, Q and U using A-configuration data only. A straightforward Clean/self-calibration cycle was used without the aid of VTESS in this case.

All the radio images were made on an 0.05 arcsec grid, and re-constructed using a synthesized elliptical Gaussian beam of 0.40 × 0.27 arcsec with major axis in position angle 35°. This gives a noise level in Stokes I of ~40 μJy beam^{-1} from both the A- and C-arrays. The percentage-polarization and apparent Magnetic Field Position Angle (MFP) images were computed using 100 × (Q^2 + U^2)^{1/2}/I and 1/2 tan^{-1}(U/I) + 90°, respectively. The Rician bias in the percentage polarization (Serkowski 1962) was corrected by measuring the noise levels in the Stokes Q and U images and using the POLC algorithm in the AIPS task COMB. Component fluxes were calculated by fitting two-dimensional Gaussians using the task IMFIT in AIPS.

2.2 Optical data

Optical HST images of 3C 15 were obtained on 2003 December 9 with the ACS/WFC instrument using the wide-band F606W filter and the three optical polarizers, each in a 2872 s exposure. Data were flat-fielded and bias-corrected using standard packages in IRAF/STSDAS, and CREEJECT was run to remove cosmic ray events (see Perlman et al. 2006, 1999, for further details). The ACS images were combined using multidrizzle (Koekemoer et al. 2002), allowing for corrections in the chip geometry (Anderson & King 2004). Stokes I, Q and U images were produced and combined following the guidelines in the ACS Data Handbook (Pavlovsky et al. 2005), and convolved with a σ = 1 pixel circular Gaussian. The
optical percentage-polarization and apparent MFPA images were produced as described in Section 2.1. Corrections were needed for the optical MFPA to include the HST roll-angle (244.9° for this observation) and the offset given by the camera geometry (−38.2′ for WFC, from Pavlovsky et al. 2005). The Rician bias in the percentage polarization (Serkowski 1962) was corrected using a script adapted from the Space Telescope European Coordinating Facility (ST-ECF) package (Hook et al. 2000) in IRAF, following Wardle & Kronberg (1974). The script uses a ‘most-probable value’ estimator, excluding pixels where the signal-to-noise ratio (S/N) is <0.5, or where the most probable value in the percentage polarization is negative or >100 per cent. Small corrections were made for the parallel and perpendicular transmittance of each filter.

3C 15 was also observed without the polarimeters at various times using a number of other filters and instruments aboard HST, listed in Table 1. Galaxy subtraction was performed using the tasks ELLIPSE and BMODEL in IRAF, and IMCALC in STSDAS. The optical images were subsequently read into AIPS for analysis.

2.3 X-ray data

The ACIS-S instrument on Chandra was used to observe 3C 15 on 2000 November 6 (ObsID 2178) in FAINT imaging mode, using chip S3 with a 1.7′-frame time. The level-1 X-ray data were reprocessed using CIAO 3.2.1 and CALDB 3.0.0 from the CXC to take advantage of recent calibration products. New bad-pixel files were created following the analysis ‘threads’ (online at http://cxc.harvard.edu/ciao/threads/), and a new level-1 event file was created with pixel randomization removed. Filtering for good grades (with values 0, 2, 3, 4, and 6) and excluding the interval of a short background flare resulted in a level-2 event file with a total good time of 25.95 ks.

The X-ray image was resampled by a factor of 4, to give a 0.123 arcsec pixel scale. This oversamples the point spread function (PSF) of Chandra, which is 0.65 arcsec for our observation. It should be noted that this procedure does not increase the image resolution in any way, although performing a Gaussian smooth (0.40 × 0.27 arcsec2) on the resampled image highlights features of the X-ray jet that the eye could otherwise miss (Fig. 2a, grey-scale).

3 RESULTS

Since the absolute astrometry of radio images from the VLA is more accurate than either the optical or X-ray data, all the cores were registered to the coordinates of the radio peak (at RA = 00°37′04″11.4, Dec. = −01°09′08″46 in J2000) prior to any analysis. The optical image was shifted by (−1.14, −0.44) arcsec and the X-ray by (0, −0.22) arcsec in (α, δ). Fig. 2(a) shows the radio contours overlaid on the corrected X-ray image.

3.1 Multiwavelength morphology

The high-resolution optical image of the jet shows four knots, labelled A–D in Fig. 2(b). We adopt the nomenclature of Martel et al. (1998) – note that Leahy et al. (1997) label the radio knots differently. Radio knot A is resolved into two optical knots, A and B, in the HST image, while knot D is detected here in the optical for the first time.

Multiband intensity profiles of the jet out to knot D were created from slices 2 arcsec wide, after rotating all the images 61.5° west from north to align the inner jet with the x-axis. Galaxy subtraction was performed on the optical image (Section 2.2), and the ultraviolet intensity profile was created by first subtracting a mean background value from the UV image. The optical and UV images were then convolved with a 0.40 × 0.27 arcsec2 Gaussian to match the radio beam size and orientation. As shown in Fig. 3, the radio and optical profiles follow each other closely – the ~20 mas (~28 pc) offset between the radio and optical peaks at knots B and C is not significant, since this is only ~10 per cent of the radio beam width. However, there is a somewhat larger 0.10 arcsec (140 pc) offset between the broad-band X-ray and radio intensity maxima in the region of knot C. With 69 X-ray counts in this region, the peak should be located to better than 60 mas with Chandra; this offset is therefore only a 1.7σ detection. Thus, we regard all the peak locations of knots A–D as consistent in the radio, optical, UV and X-ray images.

The bottom panel of Fig. 3 shows width profiles transverse to the jet direction, created by fitting one-dimensional Gaussian slices every 0.1 arcsec to the radio and optical data. Measurements were taken directly from the radio image (i.e. it was not deconvolved), although as before the optical image was smoothed with a two-dimensional Gaussian to match the radio beam. The profile shows the full width at half-maximum (FWHM) of each slice, indicating that the jet is generally narrower in the optical than in the radio, except in the region around knots A and B where the widths are similar. From both panels, it is apparent that the jet becomes slightly narrower at the flux maxima. The width profiles do not extend inside 2 arcsec, as the galaxy-subtraction procedure used for the optical data introduces artefacts close to the core. A width profile was not generated from the X-ray data, since the size of the Chandra PSF (indicated on Fig. 3, bottom panel) is too large for a fair comparison at this resolution.

The first peak in the X-ray emission at the base of the jet (knot A′, first noted by Kataoka et al. (2003) and shown here in Figs 2a and 3) occurs closer to the nucleus than any other feature. This knot is located in a region where the optical and radio intensity are still weak, before peaking further downstream at knots A and B. The ultraviolet HST image also shows that the ultraviolet intensity at A′ rises faster than in the optical, which in turn rises faster than in the radio. This observation of a kpc-scale jet appearing to turn on in the
Figure 2. Left-hand panel (a): 0.40 × 0.27 arcsec^2 resolution X-band (8.4 GHz) radio contours, and percentage polarization vectors rotated by 90° to indicate the apparent magnetic field in the radio jet. Contour levels are 0.2 × (−1, 1, 4, 10, 18, 26, 36) mJy beam^−1, and a vector of length 0.5 arcsec corresponds to 100 per cent polarization. Negative contours are dashed. The jet and nucleus are also clearly seen in the X-ray image of the full Chandra energy band, resampled by a factor of 4 and smoothed with the same 0.40 × 0.27 arcsec Gaussian (shown in the heavily clipped grey-scale image). Note, however, that the point-spread function for the unconvolved X-ray image has an FWHM of 0.65 arcsec. Right-hand panel (b): high-resolution optical polarimetry from HST, where a vector of length 0.2 arcsec corresponds to 100 per cent polarization and the grey-scale indicates the fraction. Contours show the optical intensity, with levels 0.05 × (1, 1.8, 2.8, 4.2, 5.8, 11, 14.1) electrons s^−1. Polarization vectors are rotated by 90° to indicate the apparent magnetic field direction. The ACS/F606W resolution is diffraction limited at 0.06 arcsec.

Figure 3. Top panel: linear intensity profiles 2 arcsec wide along the major axis of the inner jet, normalized to unit peak intensity. The profiles are shown for the X-band radio (solid line), V-band optical (dashed; HST ACS/F606W), the STIS ultraviolet band (dot–dot–dashed line; HST NU-VMAMA/F25QTZ) and the full Chandra X-ray band (dot-dashed line). The images were smoothed with a 0.40 × 0.27 arcsec^2 Gaussian, and representative X-ray error bars are shown. Bottom panel: the FWHM of one-dimensional Gaussian slices fitted every 0.1 arcsec to the radio and optical data in the direction perpendicular to the jet show that the jet is generally narrower in the optical than in the radio. The dot–dashed horizontal line on the bottom panel shows the FWHM of the Chandra PSF.

X-ray before its first intensity flare at lower frequencies has been seen in other FR I sources (Hardcastle et al. 2002; Worrall et al. 2006, for 3C 31 and NGC 315, respectively).

Knot A provides ~40 X-ray counts, allowing us to extract a low-resolution spectrum, although the photon statistics do not permit fitting a model more complex than a simple power law. The fitting was performed using the C-statistic in XSPEC. The spectrum, shown in Fig. 4, is well fitted by a simple power law with Galactic absorption (N_H = 3.03 × 10^{20} cm^−2, obtained using the COLDEN program from the CXC) and photon index Γ_A = 2.7 ± 0.5. Despite there being no significant radio or optical emission from A', it is interesting that its X-ray spectrum is consistent with that from knot C which is bright at all wavelengths and where we argue below that particle acceleration is significant. The steep X-ray spectrum of knot A' supports the emission being synchrotron from high-energy electrons with short lifetimes, rather than from inverse-Compton scattering of CMB photons. The emission here may be coming from a region whose self-absorption frequency is above 8.4 GHz, which could explain the lack of observed radio emission from A'. If the radio-to-X-ray spectrum is the same at A' and C, then knot A' would be detected clearly in the radio. Since A' is not visible in the radio image, the spectrum of A' cannot be the same as that of knot C over the entire radio-to-X-ray band.

The region around knots A and B is the only place where the width of the jet is similar in the optical and radio images. The X-ray intensity falls to a minimum in the A/B region, whereas the optical and radio emissions show large peaks. However, knot C is clearly detected in all three wavebands, although it is unresolved in the
Chandra X-ray image. The X-ray spectrum of knot C was fitted with a broken power law by Kataoka et al. (2003), who found a photon index of 3.0 below 0.90 ± 0.18 keV and flattening to 1.5 at higher energies. An alternative fit as a single power law had Galactic absorption and a photon index $\Gamma_C = 1.7 \pm 0.4$, although in this case the reduced $\chi^2$ was 3.1 for two degrees of freedom. It is difficult to justify a complex model when fitting only ~50 counts from knot C (radius 1.3 arcsec), and our recalibrated data fit a simple power law with Galactic absorption and a photon index $\Gamma_C = 2.4 \pm 0.5$. Background subtraction used an annulus (radii 3.1 and 5.9 arcsec) around the nucleus, thus ensuring any constant surface brightness X-rays from the lobes were subtracted. The fitted spectrum, again using the C-statistic, is shown in Fig. 4, and we note a hint of the same ‘concave’ feature in the residuals at knot C mentioned by Kataoka et al. (2003). Table 2 shows the parameters of our best fit, with a C-statistic of 3.4 using four PHA bins. The spectrum shows a low-sensitivity rise at low energies, due to a relatively large number of counts (11) between 520 and 580 eV.

The size of the Chandra PSF does not allow us to add the X-ray width profiles to the bottom panel of Fig. 3. To compare the width of the jet at knot C we convolved the optical and radio images to match the Chandra resolution and fitted Gaussian profiles to slices across the knot. The full-width half-maximum at knot C was then found to be 0.59 ± 0.05, 0.74 ± 0.02 and 0.89 ± 0.01 arcsec in the matching X-ray, optical and radio images, respectively. The width of the core on these images is the same. The results suggest that knot C becomes increasingly broader from X-ray to optical to radio wavelengths.

The diffuse X-ray emission from the lobes (Kataoka et al. 2003) makes it difficult to determine the significance of the faint X-rays that we appear to detect from the outer jet. Knot D exhibits just one count, although there are three X-ray counts from knot E (Fig. 2a). With an expected background of 0.31 counts over the whole Chandra band at knot E, the Poisson probability of obtaining three counts where 0.31 are expected is 0.36 per cent, implying a significant detection.

Table 2. Best-fitting parameters for the X-ray spectra of knot A’ and knot C in 3C 15.

| Knot | Photon index$^a$ | 1 keV Normalization$^b$ | C-statistic | PHA bins | Fit$^c$ (per cent) |
|------|-----------------|------------------------|-------------|----------|------------------|
| A’   | 2.7 ± 0.5       | $1.7^{+0.5}_{-0.3} \times 10^{-6}$ | 3.7         | 5        | 39.4             |
| C    | 2.4 ± 0.5       | $2.3^{+0.6}_{-0.3} \times 10^{-6}$ | 3.4         | 4        | 49.8             |

$^a$Errors are 90 per cent for one interesting parameter; $^b$units are photons cm$^{-2}$ s$^{-1}$ keV$^{-1}$. Errors are 1σ for two interesting parameters; $^c$goodness of fit, estimated using Monte Carlo methods. A good fit is indicated by values near 50 per cent, while very low percentages suggest the data are overfitted.

Two counts have energies less than 1 keV, although the third is above 8.5 keV and so is likely to be part of the particle background. Repeating the analysis for the same two counts on a 0.3–6 keV image gives a lower background of 0.13 counts, but with a higher chance detection of 0.74 per cent.

Fig. 3 shows the jet staying of constant width or narrowing slightly in the optical as it widens in the radio. The upstream edges of knots A and B are slightly brighter in the optical than in the radio, while the situation is reversed at the downstream edges – similar behaviour has been observed by Perlman et al. (1999) in knots in the M 87 jet. Downstream of the X-ray peak at knot C, the jet exhibits a kink of approximately 20° in both the optical and radio maps. Although the radio jet is seen to extend further and change direction again (twice), the optical emission fades rapidly after knot C, and little optical emission is detected after knot D.

3.2 Jet polarimetry

The high-resolution Stokes $I$, $Q$ and $U$ HST images were first convolved to match the size and orientation of the radio beam before comparing the optical and radio data. The structure of the jet’s apparent magnetic field is indicated in the optical and radio maps in Fig. 5, where the polarization vectors have been rotated through 90°. Although this is common practice, these vectors do not necessarily show the true projected direction of the magnetic field, which may shift due to relativistic aberration (Lyutikov, Pariev & Blandford 2003, and Section 4.2). With this in mind, Figs 2 and 5 show that the radio and optical apparent magnetic field vectors in the central part of the jet tend to be perpendicular to the jet ridge line from knot C outwards, but more parallel to the jet in the A/B region. Towards the edges of the jet the vectors tend to follow the flux contours. We note that Faraday rotation should be negligible at optical and 8.4-GHz radio frequencies.

High-resolution optical polarimetry (Fig. 2b) shows that the apparent MFPA is initially at about 53° ± 4° to the jet direction and...
that there are four distinct optical polarization minima in the knot A/B complex. The first, and least well-defined minimum, is a relatively large region around knot A spanning the whole width of the optical jet, after which the apparent MFPA rotates significantly to become parallel to the jet. The second minimum is more localized and occurs between knots A and B, while the third is located at the flux maximum of knot B where the apparent magnetic field changes direction again to follow the flux contours. The overall pattern of the vectors in this region is reminiscent of a thumbprint. Downstream of knot B, the apparent magnetic field becomes disordered and forms the fourth optical polarization minimum. At knot C (also the brightest X-ray feature) the apparent MFPA vectors generally align perpendicular to the jet. Knot D shows weak optical emission but exhibits similar polarization behaviour to that seen at the base of the optical jet, where the MFPA vectors are generally perpendicular to the new jet direction.

In the radio, the apparent MFPA at the base of the jet is broadly transverse, initially at about 60° ± 2° to the jet direction. Just upstream of knot A it rotates rapidly, becoming parallel to the jet, and aligns well with the optical MFPA. At knot B itself the apparent MFPA changes rapidly around the polarization minimum, making the local fields difficult to interpret. Further down the jet, the radio MFPA is generally perpendicular to the jet direction along its centre line.

Fig. 5(a) (colour scale) shows that the percentages of polarized emission seen in the optical and radio wavebands are similar throughout the jet, except in the region downstream of knot B. Here, the radio emission is significantly more polarized than in the optical, and the radio flux falls off less sharply with distance down the jet than the optical. At the base of the jet, the degrees of optical and radio polarization are almost the same (25 ± 3 per cent in the optical and 21 ± 3 per cent in the radio) and they fall together to 5 ± 1 per cent at the first minimum just upstream of knot A. The polarization ratio stays close to unity (both about 18 ± 2 per cent) between knots A and B, until the polarization direction changes at B and the apparent magnetic field traced by the optical emission becomes disordered shortly afterwards. The radio data show a polarization minimum centred at knot B. Knot C shows a similar degree of polarization in both bands of 24 ± 1 per cent, although there is a small region to the east of the flux maximum where the optical polarization decreases sharply. Knot D shows weak optical emission and is slightly more polarized in the optical (40 ± 6 per cent) than in the radio (33 ± 4 per cent).

The colour scale of Fig. 5(b) shows differences in the apparent MFPA between the radio and optical data. An error map of the apparent MFPA differences was produced by measuring noise levels in both the radio and optical Stokes Q and U images, and including a 3° systematic uncertainty in the optical polarization position angle (see the ACS Data Handbook, Pavlovsky et al. 2005, for further details). Regions where the statistical errors in the apparent MFPA are greater than 3° in the radio or 6° in the optical are blanked in Fig. 5 and are ignored in this analysis. It is clear that the apparent magnetic fields traced by both electron populations are quite similar, since the largest significant differences in field direction are only 10°.

In the knot A/B region, where the S/N is good, the radio–optical MFPA differences are as large as 10°, whereas the errors are ~4°. Towards the edges of the jet the errors in the MFPA differences increase to 7°. The downstream edge of knot B is weakly polarized...
in the radio but unpolarized in the optical. Knot C is different, as the apparent fields traced by the emission in both wavebands are generally perpendicular to the jet and are well ordered. In the centre of knot C the position angles align well (0° ± 4°), but the offset is about −10° ± 5° at the eastern edge and +10° ± 5° to the west. The angles at knot D are again about 10° apart, though we note that knot D is detected with relatively low significance in the optical data.

3.3 External gas

A radial profile of the X-ray image allows us to check for thermal emission from hot gas surrounding the core of 3C 15. Fitting a temperature to the spectrum and a beta-model to the profile provides an estimate of the thermal pressure at the position of knot C. Care must be taken to exclude the non-thermal emission from the kpc-scale radio lobes in the extraction region, since these are also detected in X-rays (Kataoka et al. 2003) and are clearly visible in the 0.3–6 keV Chandra image. Two 125° pie-slices were excluded, from position angles 270° to 35° (covering the NW lobe), and from 90° to 215° (the SE lobe). Annuuli were defined so that each contained at least 20 counts, giving a total of eight bins. There were 165 net counts out to a radius of 50 pixels (24.6 arcsec); background counts were obtained between radii of 50 and 80 pixels after applying the same exclusion criteria.

To probe for extended emission, we need to test if the profile is consistent with the Chandra PSF. The PSF is energy-dependent, and was modelled using the X-ray spectrum of the core between 0.3 and 6 keV, using the CHART and MARX software from the CXC. The spectrum of the core is best fitted by a two-component power law, using a circular extraction region of radius 1.3 arcsec. In agreement with Kataoka et al. (2003) we find the photon index of the first component is 1.5 ± 0.3, while the second component is heavily absorbed (Ne ~ 7 × 1022 cm−2) with slope 1.6 ± 0.5; χ2 = 11.5 for this fit, for n = 21 degrees of freedom. Formally the radial profile fits a model comprising only this PSF, with χ2 = 8.6 for n = 7. However, there is a trend towards positive residuals at the larger radii, suggesting the presence of a component of extended emission.

A fit to a beta-model as well as a point-source component gives χ2 = 2.4 for n = 4, where β = 1.5 and the core radius Rcore = 10 arcsec: both have large uncertainties. However, the formal significance of the extended component is low, with an F-test finding a 13 per cent probability of this improvement in χ2 from random data.

We have also used the spectral distribution of the counts in the lobe-free region to search for evidence of thermal emission. A fit using the spectral model of the core gives χ2 = 3.45 with n = 5 degrees of freedom (P = 63 per cent). Adding a RAYMOND thermal component gives a slight improvement of χ2 = 2.02 for n = 4 (P = 73 per cent; kT ~ 0.6 keV, upper limit 0.9 keV). Checking the significance of the improved fit using the F-statistic shows a 17 per cent probability of obtaining the improvement by chance. Although this is not significant on its own, it complements our independent observation of weak extended emission seen at large radii and suggests that external gas may be present at a level close to our best-fitting value. Our beta-model and temperature fits are converted into pressure profiles using the equations of Birkinshaw & Worrall (1993). We use the method of Worrall & Birkinshaw (2001) to find the uncertainty in pressure, but ultimately we treat our pressures as upper limits because of the weak evidence formally for the presence of the gas.

4 DISCUSSION

4.1 Magnetic structure?

From Fig. 5 and the different widths of the optical and radio jets (Fig. 3), it is clear that the optical- and radio-emitting electrons are not entirely co-located. The data on the jet widths and the direction of the apparent magnetic-field vectors suggest the presence of an optically bright spine and a lower-energy sheath. Spine–sheath structures in kpc-scale jets have been proposed in many other sources: Laing (1996) summarizes observational evidence for jets comprising a faster spine and a slower shear layer which decelerates due to the entrainment of external material. Jet velocity structures have also been proposed by Chiaberge et al. (2000) in the unification of FR I jets and BL Lac objects, where a highly relativistic spine is surrounded by a less-relativistic shear layer. These models require that the emission from the two components is only visible if it is beamed towards us. For a large number of sources, radio polarization measurements have shown that the apparent magnetic field is parallel to the jet near its base and that the field is generally perpendicular further out (Bridle 1984). Thus, in the region near the base of the jet, emission from the spine may be beamed out of our detectors, allowing us to see a parallel field from the shear layer. In 3C 15, the pattern of radio polarization vectors is consistent with what might be expected for a helical magnetic field in the outer component, and Fig. 6 shows a simple sketch of a possible magnetic field configuration in the inner jet based on the observed radio and optical data. We attempt to describe the 3C 15 jet using a more complex two-component model in a forthcoming paper.

Polarimetry around knots A and B shows very different behaviour to that seen at knot C. The radio polarization minimum around knot B may be an artefact of the vector geometry, where the field undergoes a rapid change of direction (a ‘lemon’; see Scheuer, Hannay & Hargrave 1977), or the observed field may simply appear to be disordered along the line of sight and we are seeing the projection of small-scale field variations. It is clear that the field undergoes some rearrangement in knots A and B: both the radio and optical polarimetry (Fig. 2) show similar abrupt changes in the apparent MFP downstream of knot A. The observations may be understood by a pattern shown in the shaded region of Fig. 6, where a helical field in the sheath and in the spine has a reduced pitch angle, possibly because of a longitudinal expansion caused by a release of energy in the jet. However, it is also clear that there is almost no X-ray emission from this region. This may be because the shock strength, or field geometry, does not allow particle acceleration to X-ray emitting electron energies, even though bright X-ray emission (in the absence

![Figure 6](https://example.com/image6.png)
of optical and radio) is seen in A'. Another possibility is that the X-ray emission is sporadic, and has now ceased in knot A.

The bright X-rays from knot C indicate that it is a region of effective particle acceleration, possibly near a strong shock. Our radio and optical polarimetry support the shock model by showing a high degree of polarized emission from this region. The theoretical maximum polarization for synchrotron radiation is $\sim 70\%$ (Westfold 1959; Pacholczyk 1970; Burke & Graham-Smith 2002) and the emissions from knot C are about 25 per cent polarized. The apparent local magnetic field at C is transverse to the jet and appears to be relatively well ordered. One way to achieve this configuration is to enhance the local field by compressing plasma (containing frozen-in field lines) at a shock front. The question is then why is there a stronger shock at this location than at any of the other knots? An alternative view is that there is no shock and the apparent projected magnetic field just becomes well ordered along the line of sight, although it is difficult to explain the relatively bright X-ray emission if this is all that is happening at knot C.

4.2 A test of a spine–sheath model

Our observations have constrained the differences in polarization position angle between the optically and radio bright regions of the jet. If these arise predominantly from regions of different velocity (as in a spine–sheath model), relativistic aberration of the polarization position angle may be large. In order to test such a model is not ruled out by the data, we attempt to model the jet as two components: a central high-velocity spine emitting optical synchrotron radiation, and an outer sheath of radio-emitting plasma. The simplest model has a magnetic field with components ($B_z, B_y$) in the jet frame, where $y$ is transverse to the jet direction and $z$ is parallel to it, and the ratio of $B_y$ and $B_z$ is constant – more complex models of the 3C 15 jet will be discussed in a later paper. Assuming a Lorentz factor $\gamma$ and an angle $\phi$ to the line of sight, $B_y = \gamma B_z$ and $B_z = |y + \sin^2\phi(1 - \gamma)| B_y$ in the observer frame. One can then define $	an \theta_{\text{proj}} = B_y / B_z$, where $\theta_{\text{proj}}$ is the projected angle of the magnetic field viewed by an observer relative to the jet, for $\phi > 0$. This may be rewritten as

$$\tan \theta_{\text{proj}} = \frac{y b'}{y + \sin^2 \phi(1 - \gamma)},$$

where $b' (= B_z / B_y)$ is the ratio of the two magnetic-field components in the jet frame. For a range of $\phi$, $b'$ and $\gamma$, we can examine the difference in $\theta_{\text{proj}}$ between an inner and outer component travelling at different speeds, and see if this can explain the difference in the polarization angle seen throughout the jet. We define $\theta_d$ as the difference in $\theta_{\text{proj}}$ between the two jet components. Values of $\theta_d$ are given in Table 3 for a range of parameter values.

Table 3. Differences in the projected angle of the magnetic field ($\theta_d$) between the fast and slow jet components. Values are calculated for a range of viewing angles $\phi$ and field configurations $b'$, and assume the outer component is moving slowly ($\gamma_o = 2$) while the inner component is highly relativistic ($\gamma_i = 10$).

| $b'$ | $\phi = 40^\circ$ | $\phi = 45^\circ$ | $\phi = 50^\circ$ | $\phi = 55^\circ$ | $\phi = 60^\circ$ |
|------|-----------------|-----------------|-----------------|-----------------|-----------------|
| 0.25 | 4/2             | 6/0             | 8/4             | 11/6            | 15/8            |
| 0.5  | 6/3             | 8/6             | 11/4            | 14/7            | 18/3            |
| 1    | 6/3             | 8/1             | 10/0            | 12/0            | 14/0            |
| 2    | 4/2             | 5/2             | 6/2             | 7/2             | 8/1             |
| 4    | 2/3             | 2/8             | 3/3             | 3/8             | 4/2             |

Leahy et al. (1997) found a jet-counter-jet flux density ratio in 3C 15 of $\sim 50$, implying that $\beta \cos \phi = 0.635 \pm 0.025$ if the flux asymmetry is entirely due to a relativistic effect. This puts a constraint on $\phi \sim 45-50^\circ$ for $\beta \geq 0.9$. If we assume the outer component is moving relatively slowly ($\gamma_o = 2$), the inner component is highly relativistic ($\gamma_i = 10$) and the jet lies at an angle of $50^\circ$ to the line of sight, we can obtain $\theta_d = 10^\circ$ if $b' = 1$. Fig. 5(b) shows differences in the polarization angle between the optical and radio data of 0 to $\sim 10^\circ$ throughout much of the jet, so this is plausible. However, the errors in our measurements of $\theta_d$ are in the range 4–5° in the brightest regions of the jet, so it is difficult to constrain the parameters $b'$ and $\phi$ using these data. In any case, we can see the simple magnetic field configuration does not describe many of the polarization features we see, such as the rapid rotations in the MFPA seen separately in the optical and radio data. Thus, we cannot explain the 3C 15 jet purely in terms of a velocity difference between the two components and such a simple field configuration – the field structure must itself vary, perhaps as in Fig. 6.

If the jet contains a highly relativistic spine and a slower outer component, the optical jet-counter-jet flux density ratio would be different to that seen in the radio if the optically emitting spine is moving much faster than the radio-emitting sheath. No counter-jet is detected in the optical image, and the optical jet-counter-jet ratio is not usefully constrained by the data: far deeper optical measurements are needed.

4.3 Models for knot C

The X-ray spectral fits of Fig. 4 were obtained using calibration products from the CXC which model the decline in the quantum efficiency of the Chandra ACIS detector at low energies. Consistent with this, our X-ray spectrum of knot C is steeper than that reported in earlier work (Kataoka et al. 2003), and we adopt the new value of $\Gamma_c = 2.4 \pm 0.5$ for the photon index in this analysis. The result disfavours the SSC emission mechanisms that were previously suggested for knot C, since SSC would have $\Gamma_c \sim 1.7$, and we focus instead on modelling the spectrum using only synchrotron radiation.

Radio, optical and X-ray flux densities at knot C were derived directly from the images, and are listed in Table 1. These data were used to fit synchrotron spectra to the knot emission using the code of Hardcastle, Birkinshaw & Worrall (1998a). We find magnetic field strengths on the assumption that the radiating electrons and magnetic field are in equipartition, which is roughly equivalent to the source radiating with minimum total energy, and that relativistic beaming is negligible.

The derived spectrum (Fig. 7) shows the need to introduce a break in the synchrotron spectrum of knot C, which is constrained by the X-ray photon index $\Gamma_c$. A model without a break, but with an exponential tail due to an upper cut-off in electron energy, would require an electron energy distribution with slope $p \sim 2.7$: this corresponds to a radio–optical spectral index $\alpha_o \sim 0.85$ and implies a steep radio spectral index $\alpha_r$ of the same value. Such a model also requires a steeper X-ray photon index than we observe. The data effectively rule out this scenario, since the measured optical spectral index $\alpha_o = 1.25^{+0.01}_{-0.02}$ is much steeper than the predicted value of $0.85$.

A model that includes a power-law break fits the data much better. We have constructed a synchrotron spectrum to fit the data using an electron power law of energy slope $p = 2.26$, breaking by 1.0 at a Lorentz factor $\gamma_{\text{brk}} = 8.0 \times 10^3$; this is in line with models of acceleration at strong relativistic shocks, which predict $p = 2.23$ (Achterberg et al. 2001) and $\Delta p = 1.0$ under a simple cooling assumption. This would also imply a radio spectral index
on 27 July 2018

Figure 7. Spectra for knot C, comparing equipartition models of synchrotron radiation (solid line), synchrotron self-Compton emission (dashed line) and inverse Compton scattering of the microwave background radiation (dotted line). Left-hand panel (a): simple power-law electron spectrum (slope $p = 2.74$) with high-energy cut-off at $y_{\text{max}} = 1.2 \times 10^7$. Right-hand panel (b): power-law electron spectrum with $p = 2.26$, $\Delta p = 1.0$ at $y_{\text{brk}} = 8.0 \times 10^5$.

Table 4. Synchrotron fitting parameters for the spectrum of knot C, assuming equipartition. A fitted spectrum for each model is shown in Fig. 7.

| Parameter (a) | Power law | | Parameter (b) | Break of $\Delta \alpha = 0.5$ | |
|--------------|-----------|----------------|--------------|-----------------|-------------|
| $R$ (pc)     | 250       | 250            | $\gamma_{\text{brk}}$ (Hz) | $-3.5 \times 10^{-12}$ | $-8.0 \times 10^4$ |
| $y_{\text{min}}$ | 20         | 20             | $\nu_{\text{brk}}$ (MHz) | $-3.5 \times 10^{-12}$ | $-8.0 \times 10^4$ |
| $y_{\text{max}}$ | $1.2 \times 10^7$ | $1.2 \times 10^8$ | $\gamma_{\text{brk}}$ | $-3.5 \times 10^{-12}$ | $-8.0 \times 10^4$ |
| $p$          | 2.74      | 2.26           | $\Delta p$    | $-1.00$          | $1.00$      |
| $B_{\text{eq}}$ (nT) | 31         | 20             | $\delta$      | $2.2, 1.7 \times 10^{-12}$ | $1.2 \times 10^{-12}$ |
| $\nu_{\text{sync}}$ (J m$^{-3}$) | $3.7 \times 10^{-10}$ | $1.6 \times 10^{-10}$ | $\delta^2$ (e.g. Worrall & Birkinshaw 2006), and this may be estimated using the constraint $\beta \cos \phi = 0.635 \pm 0.025$ provided by Leahy et al. (1997) based on the measured jet to counter-jet flux ratio on the assumption of twin jets that are intrinsically the same. Within the allowed ranges, $\delta$ cannot be less than $\sim 2.2$, which means the knot will still be overpressured by at least a factor of 10. It is possible that the two jets are intrinsically different and that the asymmetry is not simply due to beaming. Indeed, we already noted in Section 1 the evidence that the northern jet is FR I-like while the southern is FR II-like. However, taking the jet-counter-jet results at face value, our observations suggest the knot is likely to be a temporary feature in a state of expansion.

We note again that there is a small offset (0.14 kpc) between the positions of the intensity maxima at knot C in the X-ray and radio images. Although this detection is barely significant (less than 2$\sigma$) in the case of 3C 15, a similar offset has been observed in other nearby jets where the X-ray emission peaks closer to the nucleus (e.g. $0.35 \pm 0.1$ arcsec or $0.21 \pm 0.06$ kpc in 3C 66B, as reported by Hardcastle et al. 2001). If it is real, it may be the result of radio-emitting plasma being swept downstream, since the long lifetime of radio synchrotron emission would allow us to observe it at some distance from the shock front. Strong acceleration (to X-ray emitting energies) may only be permitted at the upstream edge of the shock. The other peculiar feature at knot C is the small ($<0.1$ arcsec) offset between the X-ray and radio/optical flux maxima in the direction transverse to the jet. Unfortunately, the resolution of Chandra does not allow us to claim that this offset is significant.

5 SUMMARY

The bright, northern jet in 3C 15 shows similar characteristics to other FR I class objects in showing a rich variety of different behaviours along its length. The base of the jet near knot A’ is...
 principally seen at high energies, in the X-ray and ultraviolet, before the optical and radio emissions turn on at knots A and B. Such behaviour is seen also in 3C 31 (Hardcastle et al. 2002) and NGC 315 (Worrall et al. 2006). With matched beams, the jet is also consistently narrower in the optical than it is in the radio for much of its length, suggesting that it is stratified. The exception is the A/B region, where the optical and radio jets are of similar width and brightness, although the region is not seen in X-rays. Throughout the jet, flux maxima appear to be accompanied by ‘pinches,’ suggesting a new component of emission is appearing in the centre of the jet and making it seem narrower. Optical and radio polarimetry around A and B show polarization minima near flux maxima in both bands, also seen in parts of the M 87 jet (Perlman et al. 1999). At knot A there is a significant change in the magnetic field position angle, where the apparent field changes from being broadly transverse to the jet to being broadly parallel to it.

We have proposed a simple model of the synchrotron-emitting jet in 3C 15, consisting of an energetic, high-velocity spine and a radio-emitting sheath. However, the data do not allow us to constrain usefully the velocities of the flow. Using a simple magnetic structure we have checked that large velocity differences between a spine and a sheath would not produce a difference in radio and optical polarization position angles larger than we observe. The A/B region shows a greater variety of polarization structure than seen in the rest of the jet, suggesting that a particularly complex field configuration and/or velocity structure is present. Detailed magnetic modelling of the jet is deferred to a later paper. We note that 3C 15 has an unusual radio morphology, where the northern jet is dissipative and appears FR I-like, while the counter-jet powers a ‘warm-spot’ in the southern radio lobe and shows classic FR II characteristics. For this reason we question the assumption that both jets are intrinsically the same, and that the observed flux asymmetry is entirely due to relativistic beaming: future models would then lose the constraint on $\beta \cos \phi$.

Knot C is bright across the X-ray, optical and radio bands, and exhibits a high degree of optical and radio polarization where the magnetic-field position angle is relatively well aligned in both components. We interpret these characteristics as the signatures of a strong shock with a well-ordered magnetic field, and high-energy emission indicates that it is a region of effective particle acceleration. Our synchrotron spectral model with equipartition magnetic field requires a break in the electron spectrum at $\gamma_{brk} = 8.0 \times 10^4$. The equipartition magnetic field of 10–20 nT (depending on jet speed) implies knot C is overpressured by ~15–60 compared with the thermal pressure from external X-ray emitting gas. This suggests knot C is a temporary, expanding feature. Knot C is suitable for more detailed examination, since it is the only part of the jet showing emission in all wavebands.

Optical knot D is detected for the first time in our long HST ACS/F606W+POL exposure, and shows a similarly high degree of polarization as knot C. Knot D is slightly more polarized in the optical than in the radio, although its optical emission is much weaker. Knot D is not detected in our Chandra observation.

These results form part of an ongoing investigation into the magnetic environment of the jets of radio galaxies. 3C 15 is one of several sources with optical synchrotron jets (including 3C 66B, 3C 78, 3C 264, 3C 346 and 3C 371) where multiband polarimetry is being assembled. Together with M 87, 3C 15 is one of the few objects with optical synchrotron jets and suggests knot C is a temporary, expanding feature. Knot C is suitable for more detailed examination, since it is the only part of the jet showing emission in all wavebands.

Future multifrequency radio observations and modelling will provide further insight into the structure of the jet, the nature of particle acceleration, and how these relate to magnetic field geometry.

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