Optical Constants and Band Gap Evolution with Phase Transition in Sub-20-nm-Thick TiO$_2$ Films Prepared by ALD

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Abstract

Titanium dioxide (TiO$_2$) ultrathin films with different thicknesses below 20 nm were grown by atomic layer deposition (ALD) on silicon substrates at 300 °C. Spectroscopic ellipsometry (SE) measurements were operated to investigate the effect of thickness on the optical properties of ultrathin films in the spectra range from 200 to 1000 nm with Forouhi–Bloomer (F–B) dispersion relation. It has been found that the refractive index and extinction coefficient of the investigated TiO$_2$ ultrathin film increase while the band gap of TiO$_2$ ultrathin film decreases monotonically with an increase in film thickness. Furthermore, with the purpose of studying the temperature dependence of optical properties of TiO$_2$ ultrathin film, the samples were annealed at temperature from 400 to 900 °C in N$_2$ atmosphere. The crystalline structure of deposited and annealed films was deduced by SE and supported by X-ray diffraction (XRD). It was revealed that the anatase TiO$_2$ film started to transform into rutile phase when the annealing temperature was up to 800 °C. In this paper, a constructive and effective method of monitoring the phase transition in ultrathin films by SE has been proposed when the phase transition is not so obvious analyzed by XRD.

Keywords: TiO$_2$ ultrathin film, Atomic layer deposition, Spectroscopic ellipsometry, Rapid thermal annealing, Phase transition

Background

Titanium dioxide (TiO$_2$) became a promising material in different applications for its excellent optical and electrical properties and chemical stability such as large band gap, high refractive index, high dielectric constant, and highly active surface [1–4]. Traditionally, TiO$_2$ pigment has almost been applied to every kind of paint due to its high refractive index [5, 6] and used as photocatalyst in the process of sterilizing, deodorizing, antifouling, and so on, which can convert light energy into electrical energy and chemical energy [6–8]. Moreover, the high dielectric constant ($k \sim 80$) of TiO$_2$ allows it to take the place of traditional silicon dioxide (SiO$_2$), used as capacitors in dynamic random access memory (DRAM) devices or ultrathin gate dielectric layers in field-effect transistors (FET) [9, 10]. Now, ultrathin TiO$_2$ layers as a barrier with a mean thickness of <3 nm could enhance photovoltaic performance of the inverted organic solar cell, especially short-circuit current ($I_{sc}$) and power conversion efficiency (PCE) [11]. Furthermore, metalenses at visible wavelengths with efficiencies as high as 86% have been demonstrated recently by using TiO$_2$ materials, in which TiO$_2$ could overcome the challenge of the high intrinsic losses in the visible range and realize the highly efficient metasurfaces in this region [12]. TiO$_2$ has been one of the most studied materials in the last decades, and numerous research concerning TiO$_2$ bulks and films have been already reported [1–4]. However, the research on the optical properties of TiO$_2$ ultrathin films, especially below 20 nm, is still rare. Thus, detailed studies on the optical properties of sub-20-nm TiO$_2$ films have become very important to the miniaturization of integrated photonic devices, the...
performance of solar cell devices, and even the application of metalenses [11–13].

TiO$_2$ thin films can be prepared by various methods such as electron beam evaporation, laser-assisted evaporation, chemical vapor deposition, sol–gel process, sputtering, and atomic layer deposition (ALD) [14]. Among them, the ALD method has been usually adopted to grow ultrathin and high-$k$ dielectrics owing to its advantages over other

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**Fig. 1** AFM micrographs of as-deposited TiO$_2$ ultrathin films with different thicknesses. **a** 50 cycles. **b** 100 cycles. **c** 200 cycles. **d** 300 cycles. **e** 400 cycles. **f** 500 cycles. **g** 600 cycles. **h** Trend chart of roughness and thickness for the seven samples.
methods in completely precise thickness control, low processing temperature, low impurity content, no line-of-sight depositions, conformal coating capability on complex-shaped structures, and excellent thickness uniformity over large deposition area [1, 3, 15–17].

This work is focused on the study of optical properties of TiO₂ ultrathin film, whose thickness is less than 20 nm. To achieve high-quality TiO₂ ultrathin films, the ALD method has been employed to deposit samples on single crystal Si substrates. Furthermore, we investigate those films mainly by spectroscopic ellipsometry (SE), a powerful non-destructive and sensitive technique. The optical constants and optical band gap of the TiO₂ ultrathin film are obtained, and the influence of nano size and temperature on the optical properties is also revealed. These results will be helpful to the applications of ultrathin TiO₂ in optoelectronic semiconductor devices such as memory, field-effect transistors, and inverted organic solar cells. What is more, a novel method to monitor the phase transition in ultrathin films is proposed by deducing from the band gap evolution.

Methods
TiO₂ ultrathin films were fabricated on Si (100) substrates by ALD (Picosun R-series, Espoo, Finland). The substrates were heated using a resistive heating plate, providing temperatures up to 300 °C. Titanium tetraisopropoxide (TTIP) was the precursor for titanium, and H₂O was the precursor for oxygen. The bubbler containing TTIP was heated to 80 °C. High purity N₂ gas was used to purge the reactor chamber after each precursor pulse. Each ALD cycle consists of four steps: first, 0.5 s to pulse TTIP; then, 10 s to purge the chamber; next, 0.1 s to pulse H₂O as the second reactant; eventually, 10 s to evacuate H₂O [18].

After deposition, the as-deposited films were annealed by a rapid thermal process (RTP; AS-ONE, Montpellier, France) system at the temperatures of 400–900 °C with an increment of 100 °C in N₂ atmosphere. Then, spectroscopic ellipsometry (SE; J. A. Woollam Co. M2000X-FB-300XTF, Lincoln, NE, USA) measurements were performed in order to examine the influence of microstructure characteristics on the optical properties of the films. All the films were characterized before and after annealing in the wavelength range from 200 to 1000 nm at the incident angle of 65 °C. The surface morphologies of films were studied using atomic force microscopy (AFM; Bruker Dimension Icon VT-1000, Santa Barbara, CA, USA) in tapping mode. The crystalline structures of films were also examined by X-ray diffraction (XRD; Bruker-AXS D8) and transmission electron microscope (TEM; FEI Tecnai G2 F20, Hillsboro, OR, USA). Besides, the reflection spectra (Lamda 950; PerkinElmer Instruments Co.) were measured to verify the band gap evolution and support the SE results.

Results and Discussion
The TiO₂ ultrathin films with different thicknesses were obtained by controlling the numbers of ALD cycles from 50 to 600 cycles. In order to identify the quality of as-deposited films and make SE measurements more effectively in characterizing the samples, information concerning the structure and morphology is an essential prerequisite. This information is conductive to establish the optical model and adopt a suitable dispersion law for calculating dielectric function in SE process [19, 20]. In consequence, the AFM, XRD, and TEM results of the as-deposited films were analyzed firstly.

The 3D AFM micrographs (scanning area 5 μm × 5 μm) are shown in Fig. 1. The surface morphologies of all films are smooth with different root mean square (RMS) roughness values (very from 0.03 to 1.23 nm), which indicates that TiO₂ ultrathin films were well fabricated (Fig. 1h). The small surface roughness can reduce the light scattering caused by rough surface in SE measurements [3].

![Fig. 2 a XRD patterns for all films of different cycles grown on Si (100) substrates. b TEM micrograph for TiO₂ ultrathin film of 600 cycles](image)

Table 1

| Thicknesses of TiO₂ ultrathin films calculated by SE |
|---------------------------------------------------|
| ALD cycles | 50  | 100 | 200 | 300  | 400  | 500  | 600  |
| Thickness (nm) | 2.55 | 3.45 | 6.05 | 9.72 | 13.90 | 16.97 | 20.61 |
The XRD patterns of all films with different thicknesses are given in Fig. 2a. The films, deposited below 300 ALD cycles, do not show any XRD peaks of TiO$_2$, indicating those films have low crystallinity or even are amorphous in nature because TiO$_2$ nanostructures in early ALD process evolve from amorphous layers to amorphous particles to metastable crystallites and finally to stable crystalline forms, which is a manifestation of the Ostwald–Lussac law [16]. When the ALD cycles are above 400, TiO$_2$ ultrathin films begin to exhibit an anatase (101) peak at $2\theta = 25.4^\circ$ [21]. The intensity of anatase (101) peak is found to increase with increasing cycles, showing that...
cycles are above 400. The TEM result of 600 cycles TiO$_2$ RMS roughness of ~1 nm is observed in Fig. 1 when the state to crystalline state as implied in Fig. 2a, an increased on account of the phase transformation from amorphous with the increasing thickness in Fig. 1h [3]. Furthermore, also explain the increasing surface RMS roughness varying graphs and the cross-sectional structure shown in TEM TiO$_2$ films are very small according to the AFM micrographs, an optical model comprising air/TiO$_2$/Ti$_x$. Si$_3$O$_2$/Si is established in the fitting process to reduce the uncertainty of fitting [25].

The Forouhi–Bloomer (F–B) dispersion model is considered to describe the optical constants of TiO$_2$ [23]. The F–B dispersion model is of benefit to determining the refractive index $n$ and extinction coefficient $k$ values accurately, which could provide a decent description of the excitations near the absorption threshold in disordered dielectrics. F–B dispersion model is described as follows [23, 26]:

$$n(E) = n(\infty) + \sum_i B_i E + C_i$$

$$k(E) = \sum_i A_i (E - E_g)$$

where $n(\infty)$ is the refractive index when photon energy $E \rightarrow \infty$, $E_g$ is the band gap of TiO$_2$, $B_i = \frac{\lambda_i}{Q_i}$ $$\left[ -\frac{B_i^2}{2} + E_g B_i - E_g^2 + C_i \right]$$, $C_i = \frac{\lambda_i}{Q_i} \left[ (E_g^2 + C_i) \frac{B_i^2}{2} - 2E_g C_i \right]$, $Q_i = \frac{1}{2} (4C_i - B_i^2)^{1/2}$, and $A_i$, $B_i$, $C_i$ are positive non-zero parameters characteristic of the medium such that $4C_i - B_i^2 > 0$. In addition, to characterize the fitting precision, the root mean square error (RMSE) is described as [23, 24]:

$$\text{RMSE} = \sqrt{\frac{1}{2N-M-1} \sum_{i=1}^{N} \left[ \psi_i^{\text{cal}} - \psi_i^{\text{exp}} \right]^2 + \left[ \Delta_i^{\text{cal}} - \Delta_i^{\text{exp}} \right]^2}$$

Table 2 Band gaps of TiO$_2$ ultrathin films

| Cycles | 50 | 100 | 200 | 300 | 400 | 500 | 600 |
|--------|----|-----|-----|-----|-----|-----|-----|
| Band gap (eV) | 3.718 | 3.615 | 3.467 | 3.443 | 3.430 | 3.422 | 3.417 |

Fig. 5 a Refractive index $n$ spectra and b extinction coefficient $k$ spectra for TiO$_2$ ultrathin films with different thicknesses after annealing at 400 °C. The insert of a shows plot of peak position versus ALD cycles. The insert of b shows plots of $(\alpha E)^{1/2}$ vs. $E$ for TiO$_2$ ultrathin films with different thicknesses after annealing at 400 °C.
The thicknesses of films calculated by SE are listed in Table 1. As we can see, all the samples except for those of 50 cycles grew at a stable speed of ~0.34 Å/cycle. In order to study the cause of different growth rates of those of 50 cycles, we also have studied the growth rate of films with ALD cycles below 50. It is found that the growth rate is still changeable and varies from 0.36 to 0.44 Å/cycle. Therefore, we hold the opinion that two reasons could cause that. On the one hand, the early ALD growth process is not stable and is in the process of nucleation. On the other, SE results exist at a certain degree of calculation error for ~0.3 nm, which could lead to a considerable calculation error to growth rate (~0.1 Å/cycle when ALD cycles are below 50).

Figure 3 displays the dispersion curves of refractive indices (n) and extinction coefficients (k). It is noticed in Fig. 3a that refractive indices increase with the increasing thicknesses of films, which is most caused by the density of films [28]. The volume ratio of air in the layer decreases when the thickness of film increases [13]. Moreover, the peak of refractive index occurs redshift with the increase of thickness, which is due to the redshift of the anomalous dispersion region (inset of Fig. 3a). Figure 3b explains that extinction coefficients increase gradually with the increasing thickness, consistent with the tendency of refractive indices. The absorption edge also shows an obvious redshift, indicating a decrease of band gap.
In order to quantify the variation of band gap, linear extrapolation of absorption coefficient $\alpha$ was conducted to determine the band gap energy evolution of TiO$_2$ films with the formula described as [23]:

$$\alpha = \frac{4\pi k}{\lambda} = \frac{K(E-E_g)^m}{E}$$  \hspace{1cm} (5)

where $k$ is the extinction coefficient, $\lambda$ is the incident wavelength, $K$ is the constant, $E$ is the photon energy, $E_g$ is the band gap, and $m$ is the number decided by the transition process, specifically divided into two kinds of situations: $m$ equals to 1/2 for direct transition and 2 for indirect transition [23, 29]. The amorphous and anatase TiO$_2$ have an indirect band gap, so the $m$ should be 2. Figure 4 shows the plots of $(\alpha E)^{1/2}$ vs. $E$ for three samples, and Table 2 lists all the band gaps of seven samples. It is obviously found that the value of band gap declines from 3.718 to 3.417 eV with the increasing thickness (Fig. 4d), as a result of quantum confinement effect [13, 30]. The decrease of the size of material leads to the increase of the band gap. Meanwhile, the smaller band gap in thicker film could cause a redshift of the anomalous dispersion region as illustrated in Fig. 3.

To investigate the temperature dependence of optical properties of TiO$_2$ ultrathin films, the samples were annealed at the temperatures of 400, 500, 600, 700, 800, and 900 °C, respectively. Figure 5a, b shows the optical constants of TiO$_2$ ultrathin films with different thicknesses after annealing at the same temperature of 400 °C. It can be found that the rapid thermal process (RTP) does not destroy the regularity of optical constants varying with thickness. The refractive index and the extinction coefficient become higher with the increase of the thickness, while the band gap of TiO$_2$ ultrathin films appears to have an opposite trend, as inferred from the inset of Fig. 5b.

Figure 6 displays the reflection spectra of TiO$_2$ ultrathin films before and after annealing at 900 °C. It can be seen clearly that the absorption edge sinks after annealing, especially for samples of 300, 400, and 500 cycles, indicating that the annealing process is very effective [31]. Furthermore, absorption edge has a redshift with increasing thickness before and after annealing, which illustrates the decrease of band gap. This also verifies the regularity of band gap evolution changing with thickness obtained via SE before.

With the purpose of studying the variation of optical properties under different annealing temperatures, samples of 600 cycles were selected and annealed in the range of 400 to 900 °C with an increment of 100 °C. As can be seen in Fig. 7a, absorption edge suddenly presents a shift and the band gap of TiO$_2$ ultrathin films decreases suddenly (inset of Fig. 7a) when the films were annealed at 800 and 900 °C. Then, the point-by-point data inversion method is employed to verify the accuracy of the reduction of band gap, as shown in Fig. 7b. It is found that the annealing temperature of 800 and 900 °C do cause a decrease of band gap.

Meanwhile, samples of 500 and 300 cycles after annealing were also selected to conduct SE analysis, as shown in Fig. 7c, d. The TiO$_2$ film of 500 cycles also appears to have a sharp decrease of band gap at 900 °C (inset of Fig. 7c), while the film of 300 cycles does not. It is conjectured that crystalline phase has been changed from anatase to rutile phase by high temperature annealing for the samples of 600 and 500 cycles, while the samples of 300 cycles are still amorphous [4, 32]. According to the previously reported research, the band gap of anatase bulk TiO$_2$ is 3.23 eV, while that of the rutile bulk TiO$_2$ is 3.02 eV [5], which is in accordance with the decrease of band gap described above, whereas there is no such phenomenon in the TiO$_2$ ultrathin film with ALD cycles fewer than 300, owing to no crystallization in extremely thin films.

Figure 8a presents the XRD patterns for films of 600 cycles after annealing, in which exists an obvious
anatase (101) peak at the annealing temperature of 400–700 °C. When the annealing temperature is as high as 800 °C, the anatase peak disappears suddenly and a rutile (110) peak emerges gradually at $2\theta = 27.5^\circ$ [4]. It has been proved that the shift of band gap in Fig. 7a, b is caused by phase transformation.

The XRD patterns for films of 500 and 300 cycles after annealing are also given in Fig. 8. For the former films, the anatase (101) peak disappears when the annealing temperature is up to 800 °C and the rutile (110) peak appears instead at 900 °C (Fig. 8b). And the latter films, as can be seen in Fig. 8c, are always amorphous before and after annealing. Thus, these results are consistent with the calculated results of SE.

Conclusions
In summary, TiO$_2$ ultrathin films with high purity were grown in a self-limited ALD growth mode by using TTIP as Ti precursors on silicon substrates at a substrate temperature of 300 °C. The TiO$_2$ layers were characterized with respect to microstructure, composition, optical constants, and optical band gap by atomic force microscopy, X-ray diffraction, reflectance spectroscopy, and spectroscopic ellipsometry.

The effect of thickness on the optical properties of TiO$_2$ ultrathin films has been investigated. The refractive index and absorption coefficient increase with the increasing film thickness, attributed to the effect of pore. On the other hand, the quantum size effect could cause the variation of band gap. Then, the as-deposited films were annealed at the temperature of 400 to 900 °C in N$_2$ atmosphere. It is found that thermal annealing does not destroy the regularity of optical constants. As for the TiO$_2$ ultrathin films with ALD cycles above 400, high temperature around 800 °C transforms the anatase TiO$_2$ to rutile TiO$_2$ via deducing from band gap evolution, which provides a novel method to detect the phase transition in ultrathin films. The results in this paper about TiO$_2$ ultrathin films will play a role in the future application of optoelectronic devices.

Abbreviations
APM: Atomic force microscopy; ALD: Atomic layer deposition; DRAM: Dynamic random access memory; F-B: Forouhi–Bloomer; FET: Field-effect transistors; PCE: Power conversion efficiency; RMS: Root mean square; RTP: Rapid thermal process; SE: Spectroscopic ellipsometry; SiO$_2$: Silicon dioxide; TEM: Transmission electron microscope; TiO$_2$: Titanium dioxide; TTIP: Titanium tetraisopropoxide; XRD: X-ray diffraction

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Authors’ Contributions
YJS performed the experiment of the TiO$_2$ ultrathin films and drafted the manuscript. RZC and XC proposed the initial work and finalized the manuscript. HZ, DHL, and WW provided guidance and assistance in the experiment. YS, YFW, and HLL participated in the design and coordination of the study. ND and LYC supervised the work. All authors read and approved the final manuscript.

Competing Interests
The authors declare that they have no competing interests.

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