Magnetic droplet nucleation boundary in orthogonal spin-torque nano-oscillators

Sunjae Chung1,2, Anders Eklund3, Ezio Iacocca1,4,5, Seyed Majid Mohseni6, Sohrab R. Sani2, Lake Bookman7, Mark A. Hoefer6, Randy K. Dumas1 & Johan Åkerman1,2

Static and dynamic magnetic solitons play a critical role in applied nanomagnetism. Magnetic droplets, a type of non-topological dissipative soliton, can be nucleated and sustained in nanocontact spin-torque oscillators with perpendicular magnetic anisotropy free layers. Here, we perform a detailed experimental determination of the full droplet nucleation boundary in the current–field plane for a wide range of nanocontact sizes and demonstrate its excellent agreement with an analytical expression originating from a stability analysis. Our results reconcile recent contradicting reports of the field dependence of the droplet nucleation. Furthermore, our analytical model both highlights the relation between the fixed layer material and the droplet nucleation current magnitude, and provides an accurate method to experimentally determine the spin transfer torque asymmetry of each device.
Magnetic solitons\(^1\) play a critically important role in nanomagnetism with the one-dimensional domain wall being the most fundamental, defining the typical scale for magnetic textures and enabling high-density magnetic storage. Two-dimensional solitons, such as vortices\(^2\)\(^-\)\(^3\), skyrmions\(^4\)\(^-\)\(^7\) and dynamical skyrmions have also received significant attention for both memory and oscillator applications\(^8\)\(^-\)\(^10\). Common to these solitons is their nonzero topological charge, which affords them particular stability in extended films. In addition to such topological solitons, there also exists a family of nontopological and intrinsically dynamical solitons, of which the two most recent experimental examples are the spin wave bullet\(^1\(^1\)\(^-\)\(^1\(^6\)\) and the magnetic droplet\(^1\(^7\)\(^-\)\(^2\(^5\)\), with very high amplitudes of self-localized spin waves at frequencies relevant for microwave applications.

Magnetic droplets (droplets from here on) were suggested in 2010 (ref. 17) as a dissipative analogue of conservative magnon drops introduced in the 1970s\(^2\(^6\)\(^-\)\(^2\(^7\)). Magnon drops can exist in magnetic thin films with perpendicular magnetic anisotropy (PMA), where the PMA leads to an attractive force between the magnons. In the absence of damping, magnons can condense leading to a partial magnetization reversal and a precessing boundary with an envelope given by a balance between anisotropy and exchange. Although real magnetic materials always exhibit non-zero damping, spin transfer torque (STT)\(^2\(^8\)\(^-\)\(^2\(^9\) can locally cancel the damping in devices known as nanocontact spin-torque oscillators (NC-STO)\(^2\(^2\)\(^-\)\(^3\(^2\)\(^-\)\(^3\(^3\)\(^-\)\(^3\(^4\). Following the first NC-STOs with PMA free layers\(^3\(^3\)\(^-\)\(^3\(^4\), droplets were finally demonstrated\(^1\(^9\) in 2013.

Although droplet theory\(^1\(^7\) has predominantly been applied to all-perpendicular spin valves, where both the free and fixed layer have strong PMA, experiments\(^1\(^9\)\(^-\)\(^2\(^5\) have used NC-STOs with in-plane fixed layers, for which the current–field phase diagram of the droplet qualitatively differs from the theoretical all-perpendicular case. Although experiments and theory both show a linear field dependence of the droplet nucleation current at high perpendicular fields, where the fixed layer is fully saturated out of plane\(^2\(^3\), the droplet nucleation current at low fields instead scales well with the perpendicular component of the spin polarization\(^1\(^9\), and acquires an inverse applied field (1/H) dependence. However, at intermediate fields, both these descriptions break down\(^2\(^1\).

In the following sections, we study these opposing trends by first mapping out the complete and detailed current–field phase diagram for droplet nucleation in a wide range of NC size, and then deriving a theoretical model that includes both the applied field, and the field-dependent perpendicular component of the fixed-layer spin polarization. We find an excellent agreement between model and experiment, including the existence of a minimum droplet nucleation current at intermediate fields.

**Results**

**Orthogonal NC-STO characterization.** The investigated devices are orthogonal NC-STOs (Fig. 1a) with a perpendicularly magnetized Co/Ni free layer, and an in-plane magnetized Co fixed layer (see ‘Methods’ section). The Co/Ni free layer has a saturation magnetization \(M_s\) of \(\mu_0 M_s = 0.9\) T and a PMA field of \(\mu_0 H_{\text{K}} = 1.35\) T, where \(\mu_0\) is the permeability of free space; the Co fixed layer has a saturation magnetization of about \(\mu_0 M_{\text{s-f}} = 1.6\) T. Figure 1b shows the field-dependent NC-STO magnetodynamics for a NC radius of 40 nm, where the perpendicular field \(\mu_0 H\) was swept from 0.05 to 0.85 T at a constant device current of \(I_{\text{dc}} = -7.7\) mA, where the negative current polarity indicates electrons flowing from the free to the fixed layer. For low magnetic fields, a faint signal is observed, corresponding to moderate-angle precession close to the ferromagnetic resonance frequency\(^3\(^3\)\(^-\)\(^3\(^4\). Above a critical field of about 0.48 T, a sudden frequency drop and a dramatic increase in microwave power (red data points in Fig. 1d) are observed, marking the nucleation of a droplet. A similar droplet nucleation transition is observed

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**Figure 1 | Orthogonal NC-STO characterization.** (a) Schematic of the orthogonal NC-STOs showing a pseudo-spin-valve composed of a Co fixed layer, a Cu spacer and a Co/Ni free layer with perpendicular magnetic anisotropy. The current enters the stack through a nanocontact (NC). The field \(H\) is applied perpendicularly to the plane. (b,c) Representative power density spectra as a function of field magnitude and current are shown in b and c, respectively. Droplet nucleation is observed as a frequency drop accompanied by a dramatic increase in power. The nucleation can also be monitored by a jump in resistance, as shown by the yellow data in b and c. (d,e) Show corresponding microwave power integrated around the main high-frequency peak (red) as well as in a low-frequency region from 0.1 to 1 GHz (black). Both the main signal power and the onset of low-frequency dynamics are clear signatures of droplet nucleation.
in Fig. 1c,e as a function of current in a constant perpendicular field of $\mu_0 H = 0.625 \, T$. The yellow line in Fig. 1b,c shows how the NC-STO magnetoresistance (MR) exhibits a step-like increase at the droplet nucleation stemming from the partial reversal of the free layer magnetization underneath the NC. The nucleation transition can also be detected by measuring the integrated microwave noise power between 0.1 and 1 GHz, black data points in Fig. 1d,e. This technique is based on the fact that broad, low-frequency features in the spectrum can be related to random transitions between different dynamical regimes. In our experiments, we hypothesize that only thermally driven spin waves and droplets are supported (corroborated by the theory given in ref. 17), suggesting that the appearance of low-frequency noise is related to the nucleation and drift instabilities of droplets. This conclusion is supported by the good agreement between the MR and microwave noise power techniques to detect a droplet, as shown in Fig. 1d,e. These are particularly useful at high fields, where the excited microwave frequencies surpass the bandwidth of our low noise amplifier (30 GHz) and spectrum analyzer (40 GHz).

Magnetoresistance measurement. Detailed MR measurements for an NC with a radius of 40 nm are plotted in Fig. 2 as a function of both field and current. Figure 2a shows field-dependent sweeps from 0.05 to 2.05 T using a field step of 0.01 T. In between each field-sweep, the current is varied in steps from $0.05 \, mA$ to $2.05 \, mA$ with data from each sweep vertically offset for clarity. Filled triangles indicate droplet collapse points extracted from Fig. 2a,b can now be plotted in Fig. 2a together with the same analysis carried out on three additional NCs with nominal radii ranging from 35 to 50 nm. Clearly, the field-dependent scans (hollow triangles pointing sideways) and current-dependent scans (solid triangles pointing up) complement each other smoothly, justifying the uniqueness of the droplet nucleation conditions. Two trends can be noticed: at low fields, the nucleation current decreases as a function of field, which is consistent with previous reports in which the nucleation current was shown to be dominated by the perpendicular component of spin-polarized current, obeying a $1/|H|$ dependence; at high fields, the dependence is linear—in strong contrast to the predicted $1/|H|$ dependence but in good agreement with numerical predictions. At field and current conditions outside of the nucleation boundary, droplet renucleation is however no longer possible, and as a consequence, most of the collapse fields in Fig. 2a can be used to trace out the high field part of the nucleation boundary.

Figure 2b shows the corresponding current-dependent sweeps using a step of $-0.02 \, mA$, while the field is increased between each sweep from 0.5 to 2.0 T in steps of 0.05 T. The obtained MR data are again plotted with a vertical offset for clarity. For low field magnitudes, where MR steps are not as easily observed, we also rely on the spectral features (abrupt frequency drop, strong power increase, low-frequency microwave noise; see Fig. 1) to uniquely define nucleation. The field dependence of the nucleation current is clearly non-monotonic exhibiting a broad minimum at intermediate fields of about 0.8 T.

Figure 2 | Magnetoresistance measurements. (a,b) Show the magnetoresistance (MR) measured by sweeping either the field or current, respectively. Each MR curve is vertically shifted for clarity. The transition resistance for droplet nucleation (collapse) is shown by a solid (empty) triangle. The solid diamonds in a indicate minor MR variations after the droplet has been nucleated and can be attributed to unstable dynamics.

Magnetic droplet nucleation boundary. All nucleation and collapse points extracted from Fig. 2a,b can now be plotted in Fig. 3a together with the same analysis carried out on three additional NCs with nominal radii ranging from 35 to 50 nm. Clearly, the field-dependent scans (hollow triangles pointing sideways) and current-dependent scans (solid triangles pointing up) complement each other smoothly, justifying the uniqueness of the droplet nucleation conditions. Two trends can be noticed: at low fields, the nucleation current decreases as a function of field, which is consistent with previous reports in which the nucleation current was shown to be dominated by the perpendicular component of spin-polarized current, obeying a $1/|H|$ dependence; at high fields, the dependence is linear—in strong contrast to the predicted $1/|H|$ dependence but in good agreement with numerical predictions.
Figure 3 | Droplet nucleation boundary. (a) Nucleation boundary found from the field sweeps (empty triangles), current sweeps (solid triangles) and low-frequency signals (solid circles) for devices with different NC radii $R_{NC}$. Fits using equation (1) are shown by solid lines using the same colour code for each $R_{NC}$. (b,c) The coefficients $A$ and $B$ are shown in b and c, respectively, as a function of NC area utilizing the same colour code as shown in a. Linear fits in b and c, shown by red dashed lines, are used to calculate the spin-torque asymmetry and efficiency.

Discussion

To understand the change in the nucleation condition trend, we rely on the stability analysis proposed in ref. 17. For the experimental conditions reported above, the uniformly magnetized state is modulationally unstable and leads to the nucleation of a droplet. Consequently, it suffices to identify the current causing the onset of this instability. This is achieved by generalizing the Slonczewski critical current condition \(^{25}\) for a material with PMA and including perturbation terms proportional to the damping parameter. By solving an appropriate boundary value problem up to first order in $\alpha$ (see the ‘Methods’ section for details), we obtain the nucleation current:

$$I_n = \alpha A H + \frac{B}{H} + C$$ \tag{1}

where $A$, $B$ and $C$ are given in the ‘Methods’ section. In contrast to previously reported models\(^{19,23}\), a term proportional to $\alpha$ is observed, only arising from a first-order correction to the Slonczewski critical current condition. Moreover, as detailed in the ‘Methods’ section, equation (1) includes the fixed layer hard axis reversal term $B/H$, applicable when the applied field does not perpendicularly saturate the fixed layer and thus must depend on material parameters. The experimental data can be fitted very well by equation (1), as shown in Fig. 3a with solid lines following the same colour coding.

To test the validity of this model, we analyse the coefficients’ dependence on the NC radius $R_{NC}$, as shown in Fig. 3b,c. Both $A$ and $B$ are found to depend on $R_{NC}$, as predicted by the analytical model and the fits shown by the dashed lines. However, we are unable to find good agreement for the current shift $C$. We argue that this disagreement stems from sample-to-sample variations and thermal excitation of magnons, which prevent the sharp spin wave onset. Indeed, the threshold current is typically one of the most variable parameters in NC-STOs and is usually estimated by projecting the thermally driven subthreshold power to zero\(^{36}\). This effect also has consequences on the zero-crossing of both $A$ and $B$ in the limit $R_{NC} \to 0$, which returns negative values from our linear fits. Despite this disagreement, the slopes of $A$ and $B$ provide valuable information for determining intrinsic STT parameters, such as the spin-torque asymmetry ($\lambda$) and efficiency ($\epsilon$). Utilizing the magnetic parameters specified above for our orthogonal NC-STO, we obtain $\lambda = 2.38 \pm 0.43$ for the spin-torque asymmetry and $\epsilon = 0.28 \pm 0.05$ for the spin-torque efficiency, obtained from equation (24), equation (25) and equation (5) in the ‘Methods’ section. The error of each parameter is obtained from 95% confidence bounds of the linear fits of $A$ and $B$ (Fig. 3a,b) and then applying error propagation.
Another characteristic of the nucleation current of equation (1) is the existence of a well-defined minimum, as observed experimentally. As noted above, the minimum occurs well below the field corresponding to a fully saturated fixed layer ($\mu_0 M_{sp}$), indicating a more involved balance between the magnetic properties of the orthogonal NC-STO. By taking the derivative with respect to the field, we obtain a minimum current $I_{min} = 2\sqrt{A B} + C$ at $H_{min} = \sqrt{B/\sqrt{A}}$. As for the calculation of the intrinsic STT parameters, we note that the slopes of $A$ and $B$ provide valuable information regarding the minimum current. Evaluating both $I_{min}$ and $H_{min}$, we obtain the proportions

$$I_{min} \propto \sqrt{J M_{sp}/M_s},$$

$$H_{min} \propto \sqrt{J M_{sp}(h_k - 1)/v},$$

where $h_k = H_k/M_s$ is the normalized anisotropy field and $v = (2 - 1)/(2 + 1)$ is the normalized asymmetry coefficient defined in the range $0 \leq v < 1$. There are two interesting conclusions that we can draw from equations (2) and (3). On one hand, the minimum current from equation (2) indicates that a lower nucleation current can be achieved by a softer fixed layer and a harder free layer while striving for a small normalized anisotropy. On the other hand, the minimum field from equation (3) is minimized by softer free and fixed layers while it requires a nonzero normalized asymmetry to be defined. These relations suggest that the magnetic materials of the pseudo-spin-valve can be engineered to optimize the minimum current while balancing the operating field value. In addition, the existence of the current and field minimum is provided by a nonzero normalized asymmetry. In other words, the change in the nucleation condition trend at fields well below $\mu_0 M_{sp}$ is direct proof of the asymmetric character of STT in metallic pseudo-spin-valves. Although theory predicts a substantial STT asymmetry in metallic pseudo-spin-valves, this has so far not been well reproduced experimentally in direct measurements, and the discrepancy has been ascribed to extrinsic device imperfections in the nanopillar geometry. In the NC-STO geometry studied here, where the lateral extent of the spin valve removes any perimeter-related imperfections, droplet nucleation offers an alternative, straightforward and sensitive method for the accurate determination of the STT asymmetry.

Methods

Sample fabrication. The orthogonal pseudo-spin-valves were deposited on thermally oxidized Si wafers using magnetron sputtering. The full stacks consisted of a pseudo-spin-valve with composition Co (6 nm)/Cu (6 nm)/Co (0.2 nm)/Ni (0.6 nm)/Co (0.25 nm) × 4 with a Ta (4 nm)/Cu (10 nm)/Ta (4 nm) seed layer and a Cu (2 nm)/Pd (2 nm) cap layer. The wafer was patterned into a 8 × 16 μm² mesa structure using optical lithography, and then coated with a 30 nm SiO₂ interlayer dielectric deposited by chemical vapour deposition. The different NC sizes were fabricated using electron beam lithography and reactive ion etching through the SiO₂. Finally, a 1.1 μm Cu top electrode was fabricated by optical lithography, sputter deposition and lift-off.

Sample characterization. The fabricated orthogonal NC-STOs were characterized in our custom probe station, allowing us to control the field magnitude and angle independently. External fields up to 2 T can be generated by an electromagnet, while the angle is controlled by tilting the sample using a mechanical rotation between the out-of-plane direction (90°) and the in-plane direction (0°). Furthermore, both d.c. and microwave measurement can be performed simultaneously. The bias current is provided by a Keithley 6221 current source from which the MB can be monitored using a Keithley 2182A nanovoltmeter. The generated a.c. voltage is decoupled by the bias using a d.c.–40 GHz bias-T. The a.c. signal is then amplified with a 0.1–30 GHz low-noise amplifier and analysed the frequency domain by a R&S FSU spectrum analyzer.

Nucleation current derivation. The nucleation of droplets in NC-STOs coincides with Slonczewski’s critical current condition, including strong perpendicular anisotropy and weakly nonlinear effects. The analytical expression for the nucleation current, equation (1), is derived by expressing the magnetization dynamics governed by the Landau–Lifshitz–Slonczewski equation as a function of the complex variable $u = m_x + i m_y$ with the small amplitude approximation $m_y = \sqrt{1 - |u|^2} \approx 1$ in the form of a complex linear Schrödinger equation (see equation (30) in ref. 17)

$$i \frac{\partial u}{\partial t} = (1 + i 2) \nabla^2 u - (h_k + h_n - 1) u - i \alpha V(u) + i \frac{\sigma V'(u)}{1 + v} u = 0.$$  

The parameters include the scaled applied field $h_k = H/M_s$, scaled anisotropy field $h_n = H_n/M_s$ and nondimensionalized parameter of spin-transfer torque $\sigma = \sigma_{sc}/h_k$, where the current density scaling is $j_0 = (\lambda^2 + 1) M^2_{sp} e_{u}/h \lambda^2$, where $e$ is the electron charge, $\mu_0$ is the vacuum permeability, $\delta$ is the thickness of the free layer, $B$ is the reduced Planck’s constant, $\lambda$ is the spin torque efficiency, $V(\rho)$ is a shifted Heaviside function and $\rho = R_{sc}/h_k$ is the scaled NC radius. Seeking a special solution in the form $u(x, t) = \rho f(\rho) \exp(-h_k - 1 + \alpha \omega_t)$, where $f(\rho)$ is a radial function, $x$ represents spatial coordinates, $\rho = |x|$, assuming $0 < \omega \ll 1$ and rescaling the spatial coordinate $\tilde{\rho} = \rho / \rho_0$, by the exchange length-scaled NC radius, we obtain the complex eigenvalue problem

$$f'' + f/\tilde{\rho} + Af + 2B \tilde{\rho} f' + B V(\tilde{\rho}) f - i \alpha C f = 0,$$

where $A = \left( R_{sc}/h_k \right)^2 / 2 \sigma$, $B = \left( R_{sc}/h_k \right)^2 / 1 + v \cos \theta t$, $C = \left( R_{sc}/h_k \right)^2 (h_n + h_k - 1 + \alpha \omega t)$, $\tilde{V}(\tilde{\rho}) = \begin{cases} 1 & \tilde{\rho} \leq 1 \\ 0 & \tilde{\rho} > 1 \end{cases}$, $\omega$ is the precessional frequency at droplet onset and $\cos \theta = H/M_{sp}$ is the angle between the free and fixed layers, given by the hard axis reversal condition. Following refs 17,35, we solve this by introducing the complex wavenumbers $k_l = \sqrt{A + B + 2(\sigma - C)}$, $k_c = \sqrt{A - i \alpha C}$, and a piecewise defined Bessel solution

$$f(\tilde{\rho}) = \begin{cases} j_0(k_0 \tilde{\rho}) & 0 \leq \tilde{\rho} \leq 1 \\ e^{-\tilde{\rho}^2 k_0^2} & 1 < \tilde{\rho} \end{cases}, \quad \epsilon = j_0(k_0 \tilde{\rho}_0) H_0^0(k_0 \tilde{\rho}_0),$$

where $j_0$ and $H_0^0$ are the Bessel and Hankel functions of the first kind, respectively. To find the two real eigenvalues $\lambda$ and $\sigma$, we require continuity of the derivative of $f$ at the NC boundary $\tilde{\rho} = 1$, leading to the complex transcendental equation

$$k_c H_0^0(k_c k_0 \tilde{\rho}_0) |j_0(k_0 \tilde{\rho}_0)| = k_0 H_1^0(k_0 k_0 \tilde{\rho}_0) |j_1(k_0 \tilde{\rho}_0)|,$$

where $j_0$ and $H_0^0$ are the Bessel and Hankel functions of the first kind, respectively.
whose real and imaginary parts determine the eigenvalues. To simplify the calculation, we solve equation (13) by expanding the wavenumbers in the small parameter $\alpha$ as

$$k_i = k_{i,0} + \alpha k_{i,1} + \cdots$$

$$\equiv \sqrt{A_0 + iB_0} + \frac{A_1 + B_1 + (iB_0 - C)}{2\sqrt{A_0 + iB_0}} + \cdots$$

(14)

$$k_i = k_{i,0} + \alpha k_{i,1} + \cdots$$

$$\equiv \sqrt{A_0 + \alpha A_1 - iC} + \frac{B_1}{2\sqrt{A_0}} + \cdots$$

(15)

where we have also expanded the eigenvalue coefficients according to

$$A = A_0 + \alpha A_1 + \cdots, \quad B = B_0 + \alpha B_1 + \cdots$$

(16)

Note that $A_0$ and $B_0$ are simply $f_0$ and $\beta$ in ref. 35. The $O(1)$ equation for equation (13) is

$$k_{i,0}H_{i,0}^{(2)}(k_{i,0})f_i(k_{i,0}) = k_{i,0}H_{i,0}^{(2)}(k_{i,0})f_i(k_{i,0}).$$

(17)

Solving equation (17) numerically gives

$$A_0 = 1.428 \ldots, \quad B_0 = 1.863 \ldots$$

(18)

The $O(\alpha)$ equation for equation (13) is

$$k_{i,1}k_{i,0}H_{i,0}^{(2)}(k_{i,0}) + k_{i,2}k_{i,1}H_{i,0}^{(2)}(k_{i,0}) = 0.$$}

This is a linear equation for $A_1$ and $B_1$ whose solution is approximately

$$A_1 \approx -3.087 + 0.815C, \quad B_1 \approx -1.518 + 1.004C.$$ (20)

Using the definitions in equation (20) gives the approximate nucleation frequency and current for a dissipative dipole

$$\omega\sim 1.428 \left( \frac{I_T}{R_{SNC}} \right)^2 + \frac{1}{Z} \left[ -1.923 \left( \frac{I_T}{R_{SNC}} \right)^2 + 0.815 (B_0 + H_k + 1) \right].$$

(21)

$$\sigma \sim (1 + vF) \left[ 1.863 \left( \frac{I_T}{R_{SNC}} \right)^2 + \frac{1}{Z} \left[ -0.084 \left( \frac{I_T}{R_{SNC}} \right)^2 + 1.004 (B_0 + H_k + 1) \right] \right].$$

(22)

We are mainly interested in equation (22). We can express this equation in terms of current density via equation (5). By implementing this change and explicitly writing the hard axis reversal condition, we get

$$I_c = \frac{\nu}{\hbar^2 R_{SNC}} \left( \frac{M_D}{H} + \frac{M_D}{H} \left[ 1.863^2 + 2R_{SNC} \left( \frac{H_k}{M_D} - 1 \right) \right] \right) \left[ 1.863^2 + 2R_{SNC} \left( \frac{H_k}{M_D} - 1 \right) \right] + \frac{1}{v_1} \frac{R_{SNC}}{M_s}.$$ (23)

which is simply equation (1) by defining the coefficients

$$A = \frac{\nu}{\hbar^2 R_{SNC}} M_s,$$

$$B = \frac{\nu}{\hbar^2 R_{SNC}} \left[ 1.863^2 + 2R_{SNC} \left( \frac{H_k}{M_D} - 1 \right) \right],$$

$$C = \frac{\nu}{\hbar^2 R_{SNC}} \left[ \frac{M_D}{H} \left( \frac{M_D}{H} \left( \frac{H_k}{M_D} - 1 \right) \right) \right] + \frac{1}{v_1} \frac{R_{SNC}}{M_s}.$$ (26)
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The affiliation details for Mark A. Hoefer are incorrect in this Article. The correct affiliation details for this author are given below:

Department of Applied Mathematics, University of Colorado, Boulder, Colorado 80309-0526, USA.

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