Theoretical insights into a colorimetric azo-based probe to detect copper ions†

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In the present study, a colorimetric azobenzene-based probe (AZO 1) was reported that exhibits high selectivity toward Cu$^{2+}$ and undergoes a red to yellow colour change upon its detection. Density functional theory (DFT) calculations were carried out to investigate the mechanism of the probe discoloration. The differences in the binding energies of complexes of 2 : 1 and 1 : 1 stoichiometry indicated that a two-step complexation process takes place as the Cu$^{2+}$ content increases. However, the calculated absorption spectra suggested that a significant colour change would only be observed for the 1 : 1 AZO 1 : Cu$^{2+}$ complex. A HOMO–LUMO electronic transition was a key factor for the blue shift of the absorption bands of the probe. Further studies indicated that solvent molecules participate in the complexation and that the presence of the o-methoxy group in AZO 1 led to formation of an octahedral complex because of the additional chelating site. A significant change in the conformation of AZO 1, namely the rotation of the N,N-di(carboxymethyl)amino group around the N–C$_{N}$ bond by approximately 90°, resulted in a larger HOMO–LUMO energy gap, and the corresponding alteration of the intramolecular charge transfer (ICT) from the N,N-di(carboxymethyl)amino group to the phenyl ring led to the observed colour change.

1. Introduction

Since the mid 1800s, azobenzene and its derivatives have been considered an important family of synthetic dyes. Numerous studies describe the synthetic methods, absorption spectra, and trans-cis isomerisation of these compounds, among other characteristics. The trans-form is generally stable and predominant. The absorption spectrum of π-conjugated trans-azo-benzene has a strong and a weak band at approximately 320 and 440 nm, respectively. However, the absorption wavelength depends on various factors such as substituents, solvents, pH, and complexation to metal ions. In addition to their use as synthetic colouring agents in the dye industry, azo compounds are promising candidates for application in molecular switches, optical memory devices, and ion detection among others.

Ion detection, especially the selective determination of heavy transition metal ions such as Cu$^{2+}$, is essential to the analysis of biological and environmental samples. Copper is an indispensable trace element for human health that plays an important role in the formation and functioning of blood cells, central nervous system, immune system, and internal organs. Although it is vital to human health in small amounts, it may be toxic in large quantities. With the continuous accumulation of copper in the body, severe health problems, such as gastrointestinal disturbance and liver or kidney damage, occur. Hence, the concentration of Cu$^{2+}$ in drinking water must be lower than 1.3 ppm (20 mM) according to the US Environmental Protection Agency.

Among many approaches to detect Cu$^{2+}$, colorimetric methods are an attractive option because of their convenience, high speed, and low cost. However, colorimetric probes for the naked eye detection of Cu$^{2+}$ reported to date are few, and include dynamic metal–organic framework receptors, amido-imine based receptors, and an azobenzene disperse dye-based colorimetric probe. A large shift in the UV-vis absorption band is an important criterion for an ideal visualization probe. In 2004, Gunnlaugsson et al. synthesized the dipotassium salts of [carboxymethyl-[2-methoxy-4-(4-nitro-phenylazo)-phenyl]-amino]-acetic acid and [carboxymethyl-[4-(4-nitro-phenylazo)-phenyl]-amino]-acetic acid (salts 1 and 2, respectively, Fig. 1). Although both salts are azobenzene-based, the absorption of salt 1 was highly affected by the presence of Cu$^{2+}$ with a large blue shift of approximately 184 nm, whereas salt 2 lacking an o-methoxy group did not detect copper ions. These findings raise the issue of whether the additional chelation site provided by the o-methoxy group is solely responsible for the different responses of salts 1 and 2 to copper ions.

Currently, computational chemistry is widely accepted by scientists in different fields as a tool to provide explanations at
2. Theoretical studies

2.1. Molecular models

Considering that salts dissociate in aqueous solutions, \{carboxymethyl-[2-methoxy-4-(4-nitro-phenylazo)-phenyl]-amino\}-acetate (AZO 1) and \{carboxymethyl-[4-(4-nitro-phenylazo)-phenyl]-amino\}-acetate (AZO 2) were used in the modelling. The two most common spatial structural models for copper ions, the planar four-coordination and octahedral six-coordination models, were adopted. As complex structures can also be formed between copper ions and solvent molecules, the participation of chloride ions and water molecules in complexation was taken into account. Based on these considerations, distinct initial complexes of 2 : 1 and 1 : 1 stoichiometry were modelled for the AZO ligands and Cu$^{2+}$.

2.2. Computational details

Geometry optimisation and frequency calculations of the molecular models were performed using B3LYP/6-31G(d,p), which enables a qualitative prediction of the absorption properties of azobenzenes.$^{2,3}$ The LanL2DZ effective core potentials and a spin-unrestricted model for Cu$^{2+}$ were employed. The absorption spectra were predicted by the time-dependent density functional theory (TDDFT) and 50 states were calculated. Solvent effects were considered within the polarizing continuum model (PCM) framework by including water in the geometry optimisation and excited state calculations. All quantum calculations were performed using Gaussian 16 programmes on a Linux system.

3. Results and discussion

Geometry optimisation and frequency calculations for AZO 1 and AZO 2 in aqueous solutions were performed to locate and verify the minima. The electrostatic potential can clarify the molecule’s reactivity since negative electrostatic potentials correspond to a high electron density and the ability to attract a proton and \textit{vice versa}.$^{2,3}$ The mapped electrostatic potential surfaces generated from the electron density cubes are illustrated in Fig. S1.$^\dagger$ The colour changed from blue to red along with the value of the electrostatic potential which varied from 0.28 to $-0.28$. As expected, the increased electron density in the vicinity of the methoxy and carboxyl groups of AZO 1 represented an additional Cu$^{2+}$ chelation site.

3.1. Complexation of AZOs and Cu$^{2+}$ in 2 : 1 stoichiometry

When the copper ion concentration was relatively low, complexation of AZOs and Cu$^{2+}$ occurred in 2 : 1 stoichiometry. The optimised structures are shown in Fig. 2, which shows (a) the complexation of AZO 1 and Cu$^{2+}$, $1 + \text{Cu}^{2+} + 1$, and (b) that of AZO 2 and Cu$^{2+}$, $2 + \text{Cu}^{2+} + 2$. For AZO 1, the oxygen and nitrogen atoms of the $N,N$-di(carboxymethyl)amino groups and the oxygen atoms of the o-methoxy groups participated in the chelation of Cu$^{2+}$. However, chelation of Cu$^{2+}$ by AZO 2, lacking o-methoxy groups, occurred only \textit{via} the oxygen and nitrogen atoms of the $N,N$-di(carboxymethyl)amino groups, resulting in an approximately square-planar coordination geometry and a “Z” or “Π” arrangement of the azo groups. The distance between Cu$^{2+}$ and the chelation site, N–O–Cu angles, and binding energies are listed in Table S1.$^\dagger$ The latter was calculated as the energy of complexation minus the energies of each molecule. A careful analysis of the relationship between structure and binding energy indicated that higher binding energy values corresponded to Cu$^{2+}$ complexes closer to square planar or octahedral geometries (Fig. 2 and Table S1$^\dagger$).

We selected the complexation of a2 and b4 with binding energies of $-223.606$ and $-213.894$ kcal mol$^{-1}$, respectively, for further study. Their UV-vis spectra are shown in Fig. 3 along with the corresponding main molecular orbitals, whereas the spectra of the other structures were depicted in Fig. S2.$^\dagger$ The absorption peak of a2 in the range of 550–650 nm was noticeably weaker than those of the other structures (Fig. 3 and S2$^\dagger$). The involved transition orbitals indicate that these peaks originate from the intramolecular charge transfer (ICT) from the $N,N$-di(carboxymethyl)amino group to the phenyl rings, rendering this ICT dependent on the spatial arrangement of the groups. In a2, slight rotation of the $N,N$-di(carboxymethyl) amino group to form an octahedral Cu$^{2+}$ complex weakened the ICT. In addition, the calculated absorption spectra suggest that no obvious colour changes accompanied the chelation of Cu$^{2+}$ by AZO 1 or AZO 2 in solution when the stoichiometry was 2 : 1.

3.2. Complexation of AZOs and Cu$^{2+}$ in 1 : 1 stoichiometry

With the increase in the copper ion content, complexation of AZOs and Cu$^{2+}$ in 1 : 1 stoichiometry takes place. Out of different initial models, optimised structures were selected for detailed studies taking into account the planar four-coordination or octahedral six-coordination of Cu$^{2+}$. The structures of $1 + \text{Cu}^{2+} + \text{Cl}^{-}$, $1 + \text{Cu}^{2+} + \text{H}_{2}\text{O}$, $2 + \text{Cu}^{2+} + \text{Cl}^{-}$, and $2 + \text{Cu}^{2+} + \text{H}_{2}\text{O}$, together with the optimised AZO 1 and AZO 2 structures are displayed in Fig. 4, whereas other optimised...
Complexation modes are presented in Fig. S3†. The chelation sites and Cu$^{2+}$ are highlighted by differently coloured spheres (blue for N, red for O, green for Cl$^{-}$, and orange for Cu$^{2+}$). The artificially added light grey plate and arrow indicate the position of the atoms in Fig. 4, which shows the participation of the coplanar O1, O2, and N atoms in the complexation of Cu$^{2+}$. Additionally, the o-methoxy group in AZO 1 forces the central copper ion to adopt the six-coordinated octahedral geometry. However, complexation of Cu$^{2+}$ by AZO 2 is different than that by AZO 1, as the lack of the o-methoxy group results in a change in the spatial location of the copper ion from the side of the azobenzene plane to its front. Due to the repulsion of the azobenzene conjugated plane, stable octahedral structures are not obtained. Instead, the four-coordinated planar geometry is acquired for 2 + Cu$^{2+}$ + Cl$^{-}$ and 2 + Cu$^{2+}$ + H$_2$O (Fig. 4(e) and (f), respectively).

Table S2† shows the binding energies in the complexes, which consist of azobenzenes, Cu$^{2+}$, and solvent particles (chlorine ions or water molecules) and have therefore two distinct binding energies. That between AZO and Cu$^{2+}$ ($\Delta E_1$), calculated as $\Delta E_1 = E_{\text{complex}} - E_{\text{AZO}} - E_{\text{copper ion + solvent particles}}$, is $-119.263, -160.862, -127.272,$ and $-174.463$ kcal mol$^{-1}$ for 1 + Cu$^{2+}$ + 2Cl$^{-}$, 1 + Cu$^{2+}$ + 2H$_2$O, 2 + Cu$^{2+}$ + Cl$^{-}$, and 2 + Cu$^{2+}$ + H$_2$O respectively, whereas the energy between Cu$^{2+}$ and solvent particles ($\Delta E_2$), calculated as $\Delta E_2 = E_{\text{complex}} - E_{\text{AZO + copper ion}} - E_{\text{solvent particles}}$, is $-32.925, -32.421, -27.833,$ and $-23.001$ kcal mol$^{-1}$ for the same complexes. The total binding energy ($\Delta E$) was calculated as the energy of complexation minus

![Fig. 2](image-url) Optimized structures of 2 : 1 stoichiometry for AZOs and Cu$^{2+}$ calculated at the levels of B3LYP/6-31G(d,p)//LanL2DZ: (a) complexation of AZO 1 and Cu$^{2+}$; (b) complexation of AZO 2 and Cu$^{2+}$. The chelation sites and Cu$^{2+}$ are all highlighted by using balls of different colors. N is in blue, O is in red, and Cu$^{2+}$ is in orange. All hydrogen atoms are not shown.

![Fig. 3](image-url) Calculated UV-vis spectra of complexation of 2 : 1 stoichiometry for AZOs and Cu$^{2+}$ of a2 and b4 which have larger binding energies than other complexation. Some main molecular orbitals were presented next to the corresponding absorption peaks.
the energies of each molecule, and were \(-241.589, -248.296, -224.407, \) and \(-222.576\) kcal mol\(^{-1}\) for \(1 + \text{Cu}^{2+} + 2\text{Cl}^{-}\), \(1 + \text{Cu}^{2+} + 2\text{H}_2\text{O}\), \(2 + \text{Cu}^{2+} + \text{Cl}^{-}\), and \(2 + \text{Cu}^{2+} + \text{H}_2\text{O}\), respectively. The values of \(\Delta E_1\) reveal that the interaction between AZO and \(\text{Cu}^{2+}\) is enhanced by water molecules more significantly than by chlorine ions. Additionally, comparison of the binding energies of AZOs and \(\text{Cu}^{2+}\) complexes of 1:1 and 2:1 stoichiometry shows that the former are more stable structures. Hence, a two-step complexation process (AZOs and \(\text{Cu}^{2+}\) from 2:1 to 1:1 stoichiometry) should occur as a result of an increase in the copper ion content.

The vertical electronic excitation energies were calculated at the TD-B3LYP/6-31G(d,p)//LanL2DZ level. The absorption spectra were artificially broadened using the GaussSum 2.2.5 software. The simulated UV-vis spectra of AZO 1, 1 + \(\text{Cu}^{2+} + 2\text{H}_2\text{O}\), AZO 2, and 2 + \(\text{Cu}^{2+} + \text{H}_2\text{O}\), and the UV-vis spectra of 1 + \(\text{Cu}^{2+} + 2\text{Cl}^{-}\) and 2 + \(\text{Cu}^{2+} + \text{Cl}^{-}\) shown in Fig. 5 and S4,†
respectively, reveal that the influence of the chlorine ions on the absorption spectra is similar to that of the water molecules. Since the latter can significantly increase the interaction between the AZO and copper ion, only the absorption spectra of Fig. 5 are analysed herein. Two distinct absorption bands of AZO 1 are calculated at 672 and 465 nm (the experimental values are 509 and 325 nm), and those of AZO 2 are at 644 and 432 nm, indicating a red shift of approximately 30 nm upon introduction of the \(o\)-methoxyl group. However, the spectra of 1 + Cu\(^{2+}\) + 2H\(_2\)O and 2 + Cu\(^{2+}\) + H\(_2\)O are distinct. The former shows an extinct peak at 366 nm and a shoulder at 416 nm. The clear blue shift with regard to the spectrum of AZO 1 explains the colour change of the solution from red to yellow. However, the absorption spectrum of 2 + Cu\(^{2+}\) + H\(_2\)O shows a weak band in the range of 500–800 nm. As the absorption intensity increases with the concentration and the solution contained more than one AZO 2, this absorption cannot be ignored in the real experiment. Since a 1 : 1 mixture of AZO 2 and Cu\(^{2+}\) absorbed in the green spectral region, no obvious colour change was observed during the experiment.

In order to explain the observed >250 nm blue shift of the AZO 1 absorption bands in contrast to the unchanged AZO 2 absorption in the range of 500–800 nm upon combining the AZOs with Cu\(^{2+}\) in a 1 : 1 stoichiometry, the major molecular orbitals involved in the transitions were examined (Fig. 6). In the case of AZO 1, the red colour results from the first lowest excited state of 672 nm, which corresponds to the HOMO → LUMO transition (98%, \(\text{O}_{\text{exc}} = 0.8804\)). The data of 1 + Cu\(^{2+}\) + 2H\(_2\)O show that the 11\(^{th}\) to 25\(^{th}\) excited states were relevant to the colour change, among which the 12\(^{th}\) and 23\(^{rd}\) excited states greatly contributed to the absorption. Specifically, the 12\(^{th}\) excited state (416 nm, \(\text{O}_{\text{exc}} = 0.3762\)) was related to the ICT from the \(N,N\)-di(carboxymethyl)amino group to the phenyl rings. Similarly, we found that the AZO 2 absorption peaks resulting from the HOMO → LUMO transition (644 nm, \(\text{O}_{\text{exc}} = 0.8679\)), ICT from the \(N,N\)-di(carboxymethyl)amino group to the phenyl rings) accounted for the red colour. A weak peak at 656 nm in the spectrum of 2 + Cu\(^{2+}\) + H\(_2\)O indicated a HOMO → LUMO\(_a\) transition (54%, ICT from the phenyl rings to the \(N,N\)-di(carboxymethyl)amino group). A shoulder at 473 nm was also observed due to the HOMO → LUMO\(_g\) transition (34%), whereas the strong peak at 407 nm results from a HOMO → LUMO\(_g\) transition (40%, ICT from the \(N,N\)-di(carboxymethyl) amino group to the phenyl rings). Hence, we infer that the HOMO to LUMO electronic transition is a key factor for colour change (or lack thereof) upon combining AZO 1 and AZO 2 with Cu\(^{2+}\) in a 1 : 1 stoichiometry. The HOMO–LUMO energy gap was calculated as \(\Delta E_{\text{H-L}} = E_{\text{HOMO}} - E_{\text{LUMO}}\). The \(\Delta E_{\text{H-L}}\) of AZO 1 and AZO 2 are 1.9 and 2.01 eV, respectively, whereas the \(\Delta E_{\text{H-L}}\) of 1 + Cu\(^{2+}\) + 2H\(_2\)O are 3.37 and 3.34 eV for the \(\alpha\) and \(\beta\) orbitals, respectively, and the corresponding values for 2 + Cu\(^{2+}\) + H\(_2\)O are 3.32 and 2.87 eV (\(\alpha\) and \(\beta\) orbitals, respectively). Clearly, the AZO 1 and AZO 2 strong bands and the 2 + Cu\(^{2+}\) + H\(_2\)O weak bands in the range of 500–800 nm were due to the small \(\Delta E_{\text{H-L}}\) (<3 eV). Hence, the presence of the \(o\)-methoxy group in AZO 1 led to formation of an octahedral copper complex. As a result, rotation of the \(N,N\)-di(carboxymethyl)amino group by approximately 90° around the \(N-C_{\text{Me}}\) bond, which in turn led to a larger HOMO–LUMO gap of approximately 3.34 or 3.37 eV related to the ICT from the \(N,N\)-di(carboxymethyl)amino group to the phenyl ring.

4. Conclusion

To investigate the mechanism of Cu\(^{2+}\) detection by AZO 1 in aqueous solution, DFT calculations at the B3LYP/6-31G(d,p)///LanL2DZ level were performed. For comparison, the related AZO 2 molecule lacking an \(o\)-methoxy group on the phenyl ring was also studied. The mapped electrostatic potential surfaces suggested the \(o\)-methoxy group in AZO 1 is an additional chelation site for Cu\(^{2+}\). Complexation of AZOs and Cu\(^{2+}\) in a 2 : 1 stoichiometry would occur at low Cu\(^{2+}\) concentrations without colour change, according to the corresponding calculated
absorption spectra. With the increase in the Cu\(^{2+}\) concentration, complexation of AZOs and Cu\(^{2+}\) in a 1:1 stoichiometry would occur. The geometry of the optimised structures revealed that the formation of an octahedral complex requires rotation of the N,N-di(carboxymethyl)amino group by approximately 90° around the N–C\(_{ar}\) bond in AZO 1. In contrast, AZO 2 lacking a o-methoxy group led to a four-coordinated, planar Cu\(^{2+}\) complex in which the N,N-di(carboxymethyl)amino group did not rotate. Further studies revealed that electronic transitions from HOMO to LUMO were the key factors in the colour changes of the solutions, thus enabling the detection of Cu\(^{2+}\). The change in the conformation of AZO 1 in the 1:1 complex is associated with a larger HOMO–LUMO gap (\(\Delta E_{H-L}\) was 3.34 and 3.37 eV for \(\alpha\) and \(\beta\) orbitals, respectively). Hence, the ICT from the N,N-di(carboxymethyl)amino group to the phenyl ring with a larger \(\Delta E_{H-L}\) results in >250 nm blue shift of the absorption bands, which corresponds to the change in the colour of the solution from red to yellow.

**Conflicts of interest**

There are no conflicts to declare.

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