Using convolutional neural networks to identify gravitational lenses in astronomical images

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1 INTRODUCTION

Gravitational lensing is caused by the mass of a foreground object, such as a galaxy or galaxy cluster, deflecting light from another distant source object, such as a galaxy or quasar. Strong gravitational lensing is rare with only a few systems expected from surveying thousands of objects (Blain 1996). The first strong gravitational lens system, QSO 0957+561, was recognized as such in 1979 when the spectra of two objects were compared and confirmed to be from the same object (Walsh, Carswell & Weymann 1979).

The Jodrell Bank-VLA (Very Large Array) Astrometric Survey (JVAS; Patnaik et al. 1992; Browne et al. 1997) and the Cosmic Lens All-Sky Survey (CLASS; Browne et al. 2003; Myers et al. 2003) have detected 22 radio loud lensed active galactic nuclei (Chae 2003). Currently, the Sloan Lens ACS Survey (SLACS) has provided the most strong lensed systems from a single survey with nearly 100 observed (Bolton et al. 2008). Other sources of strong lenses include the Kilo-Degree Survey (KiDS; de Jong et al. 2015) that uses the VLT Survey Telescope at the Paranal Observatory in Chile, the Dark Energy Survey (The Dark Energy Survey Collaboration 2005), and the Subaru Hyper Suprime-Cam Survey (Miyazaki et al. 2012), expected to observed thousands of lenses (Collett 2015). The BOSS Emission-Line Lens Survey (BELLS) have discovered at least 25 strong galaxy—galaxy gravitational lens systems with lens redshifts $0.4 < z < 0.7$, discovered spectroscopically by the presence of higher redshift emission lines within the Baryon Oscillation Spectroscopic Survey (BOSS) of luminous galaxies, and confirmed with high-resolution Hubble Space Telescope (HST) images (Brownstein et al. 2012).

Lensing systems are extremely useful cosmological tools. Lensed systems can be used to constrain the value of the Hubble constant, $H_0$, by measuring time delay (Refsdal 1964; Kochanek & Schechter 2004), which occurs because the light from multiple images has taken different paths to reach the observer, introducing a time delay. Cosmological distances are proportional to $c/H_0$, meaning $\Delta t = (1/H_0)k$, where $k$ is related to the lens mass model. If a lens model can be found then we can predict $\Delta H_0$ and infer $H_0$. Gravitational lensing is independent of the lensing object’s luminosity and depends only on the mass of the lens object and the geometry of the source and the lens relative to the observer. This makes lensing a unique tool for analysing mass distribution in the foreground lens (Treu & Koopmans 2002). Using this dependence on mass alone, and combining mass models from mass—luminosity analysis, the baryonic and dark matter mass of the galaxy can be mapped to find dark matter substructure (Metcalf & Madau 2001; Vegetti et al. 2012). Gravitational lensing conserves surface brightness (a consequence of Liouville’s Theorem) but not the angular size of the source object (Marchetti, Serjeant & Vaccari 2017), causing a magnification of the source object’s flux, if the image of the source is enlarged. This enables the observation of fainter galaxies that would otherwise be missed, including galaxies

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Future telescopes are expected to observe many more strongly lensed systems. The *Euclid* telescope (Laureijs et al. 2011) and the Large Synoptic Survey Telescope (LSST Science Collaboration et al. 2009) will bring the total number of systems above 10^5 (Oguri & Marshall 2010; Collett 2015). *Euclid* will map three-quarters of the extragalactic sky with 0.2 arcsec resolution to 24 AB magnitude (Amendola et al. 2018). Another project, the Square Kilometer Array (SKA; Rawlings & Schilizzi 2011), will take observations at a resolution of 2 mas at 10 GHz, and 20 mas at 1 GHz (Perley et al. 2009). The lensing surveys using SKA are expected to observe \( \approx 10^5 \) new radio-loud gravitational lenses (Serjeant 2014; McKean et al. 2015).

There is currently a shift in the methodology for detecting strongly lensed systems in astronomical images as numbers of lens candidates becomes much larger. Traditionally most images were found by eye. 112 lens candidates, and at least 2 certain lenses, were found in a *HST* legacy programme, looking at the COSMOS field (Faure et al. 2008; Jackson 2008). But not all searching by eye has been carried out by people working in strong gravitational lensing. The public have been tasked with finding new lens candidates through the Space Warps citizen science project (Marshall et al. 2016). Space Warps made use of volunteers analysing 430,000 images by eye to look for lensing features, via an online webpage using the Zooniverse platform. Tens of new lens candidates have been identified with the help of these volunteers, using large ground-based surveys, e.g. the Canada—France—Hawaii Telescope Legacy Survey (More et al. 2016). But with the growth of survey size, there will be too many candidates to be examined by eye.

There have been several successful methods of computational searches for lenses. Arcfinder (Seidel & Bartelmann 2007) uses pixel-grouping methods to attempt to find cluster-scale lens systems. Ringfinder (Gavazzi et al. 2014) searches for blue residuals surrounding early-type galaxies using multiband data, also there are several programmes to find arc-like shapes (Lenzens et al. 2004; More et al. 2012).

In recent years, there has been a rise in machine-learning methods to detect lenses. 56 lens candidates were found in the KiDS data set using a convolutional neural network (CNN; Petriillo et al. 2017). Machine learning methods rely on large data sets in order to train and learn, something which has become available in recent years. Once a machine has been trained, thousands of images can be classified in seconds. Speed is an important factor due to the expected \( 10^5 \) images from *Euclid* (Collett 2015). The use of citizen science could be used to create a data set of images for machine learning techniques to train on, once trained, citizen science can then be applied again to examine the output images from the machine learning technique.

In Section 2, we discuss neural networks (NNs) and why we use them for this problem. In Section 3, we discuss the simulated data we have used. In Section 4, we discuss our CNN and how we trained it, and the results are discussed in Section 5. The python code is available at github.1

2 WHY USE NNS

Computers are very effective at tasks with a limited set of rules, such as chess. However, humans are still often better at real world tasks that cannot easily be described by a set of rules, e.g.

![Diagram of a perceptron](https://example.com/diagram)

**Figure 1.** A perceptron with inputs \( x_1, x_2, x_3, x_4 \), weights \( w_1, w_2, w_3, w_4 \), bias \( b \), and output calculated from the activation function \( f \), together with the product of the weights and input and bias added.

recognizing objects. Artificial NNs are loosely inspired by how the brain works. They are made from simple computing elements with multiple inputs and one output analogous to a brain made up from neurons with dendrites and cell body receiving the inputs and axon outputting a signal. Like the brain, an NN can modify strengths of connections learnt from examples. Humans have evolved to be very fast and accurate at recognizing objects of the order of 100 ms (Thorpe, Fize & Marlot 1996). NNs, particularly CNNs, are the best available techniques in some tasks, e.g. translation and visual object recognition (LeCun, Bengio & Hinton 2015). With current technology, a trained CNN can also perform these tasks faster than humans.

NNs are built from individual artificial neurons called perceptrons. A perceptron is designed to simulate the role of a biological neuron, but with the advantage that a mathematical function can be used for activation of the neuron (Aggarwal 2014). A perceptron takes a number of inputs, applies a weight to each, sums these products, applies a bias, and then is used as input to an activation function, which then gives the perceptron’s output. Perceptrons can accept multiple inputs and apply different weights to each individual input. A perceptron with example inputs and outputs can be seen in Fig. 1. Individual scalar inputs are grouped together as a 1D vector. If we let \( x \) be the 1D vector of inputs, \( w \) be the 1D vector of weights associated with this perceptron, \( b \) be the bias, and \( f \) be the activation function, then the output \( z \) is calculated using

\[
z = f(\sum_{i=1}^{n} w_i x_i + b),
\]

where \( n \) is the number of inputs to the perceptron. In an NN, many perceptrons are grouped together to form a layer containing a few perceptrons to thousands. Layers use the outputs from previous layers as their inputs.

NNs have to be trained before they can be used. For classification problems, this involves passing many images of a known classification through the network in a process called supervised learning. The network classifies each image, and this output is combined with the true classification in a function called the loss function. A high value for the loss function means many images were incorrectly labelled by the network. The goal of training the network is to minimize the loss function over a number of passes of the training data. Each pass of the data is known as an epoch. After each epoch, the weights and biases are changed using Stochastic Gradient Descent (SGD) in order to minimize the loss function, thereby increasing the rate of correct classifications from the network. The rate at which SGD changes the weights and biases is controlled by a variable called the learning rate. There is a linear parameter which controls

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1https://github.com/A-Davies/LensCNN
CNNs have been used to solve classification problems such as digit recognition with the MNIST data base, a collection of 70 000 $32 \times 32$ grey-scale images of handwritten digits. The problem is to classify these as the digits 0 through 9. Using CNNs gives a solution with an error rate of 0.23 per cent (Ciresan et al. 2013). CNNs have also been successful in object recognition in images. The CIFAR-10 data base consists of 60 000 $32 \times 32$ colour images in 10 classes, such as truck, bird, and dog, with 6000 images per class. The error rate in this classification problem when using CNNs is lower than 4 per cent.\(^2\) An astronomy classification problem where CNNs have been used is classifying images as a star or galaxy. Here, the best network had an error rate of only 0.29 per cent for galaxies (Kim 2007; Dieleman, Willett & Dambre 2015).

3 METHODS

The task of finding strong gravitational lenses in large data sets is a problem within Euclid. Feature recognition by eye will not be fast enough to cope with the amount of data received. The Strong Lensing challenge within the Euclid consortium set up the Euclid Strong Lensing challenge. This was a challenge aimed at developing machine learning techniques to classify images as to whether containing a lens or not. The simulated data was provided by the Bologna Lens Factory.\(^1\) The images are producing using GLAMER code (Metcalf & Petkova 2014), which uses galaxies from the Millennium Simulation\(^4\) and real galaxies from KiDS as foreground lenses and background sources to produce the simulated images. More details of the lensing process can be found in Metcalf et al. (2018). The simulated images are provided as 101 $\times$ 101 pixel sized images, centred on the foreground galaxy, either containing a lensed source or not. In total 200 000 images were provided, 100 000 were Euclid VIS-like images, with $\approx 40$ 000 lenses and 100 000 were KiDS-like images, with $\approx 50$ 000 lenses. The Euclid-like space images are single-band images, very broad-band ($r+i+z$), whereas the KiDS-like images have four bands: $u$, $g$, $r$, $i$. The images have an image resolution of 0.2 arcsecond, meaning each is a 10 $\times$ 10 arcsecond square image. Examples of the Euclid VIS-like images can be seen in Fig. 3, and an example of the 4 KiDS-like bands can be seen in Fig. 4. However, our close scrutiny of the simulated images uncovered some unphysical examples. The COSMOS lenses\(^5\) were used as a comparison to test the simulations against. Examples of the COSMOS lenses can be seen in the Appendix. The band used for the COSMOS images is the HST F814W wide band. F814W covers the longer wavelength half of the VIS throughput. Visual inspection of the VIS and smoothed COSMOS images shows qualitatively similar features. Therefore, we argue that the COSMOS data set is an appropriate and interesting test of our VIS-trained network.

By comparing histograms of the Einstein radius and lens magnitudes of both the simulated Euclid VIS-like images and the real COSMOS lens images, it was found that many of the simulations

\[^{2}\]http://rodrigob.github.io/are_we_there_yet/build/classification_datasets_results.html

\[^{3}\]https://bolognalensfactory.wordpress.com/

\[^{4}\]https://wwwmpa.mpa-garching.mpg.de/galform/virgo/millennium/

\[^{5}\]http://www.staff.uni-heidelberg.de/mitarbeiter/cfaure/cosmos/
Figure 3. Samples from the 100 000 *Euclid* VIS instrument simulated images. The top row of images do not contain lenses, while the bottom row contains lenses.

Figure 4. A sample from the 100 000 KiDS-like simulated images. The images are labelled above by their corresponding wavelength band. This example does contain lensing.

had unrealistically large Einstein rings and that the *Euclid* VIS-like and KiDS-like simulations were fainter than the COSMOS lenses. Because of this, images with Einstein radii greater than 4 arcsec, and lenses towards the faint end of the *Euclid* VIS-like and KiDS-like data sets have been removed in order to create a more representative subset. Histograms showing removal of some of the *Euclid* VIS-like images to make the data set more COSMOS-like can be seen in Fig. 5. A similar histogram also shows that by removing the larger Einstein radii, the *Euclid* VIS-like images have an Einstein radius distribution similar to that of COSMOS. The same has been done for the KiDS-like data set. In total, we now have four data sets for training and five for testing that can be seen in Table 1.

4 TRAINING TO FIND LENSES

Four networks have been built, two designed to work with KiDS-like images with four filter bands as input, and two to work with *Euclid* VIS-like data with a single filter input. They have the same architecture, but have been trained on different data using data sets 1–4 from Table 1. The networks have been built and trained in PYTHON 2.7 using the NN library Keras. Keras runs on top of

Figure 5. Histograms showing the AB magnitude across three data sets. Top: Original 100 000 *Euclid* VIS-like images. Middle: Subset of *Euclid* VIS-like images designed to have the same distribution as the COSMOS lenses. Bottom: The COSMOS lenses.

Theano, TensorFlow, or CNTK back ends. We used Theano. The CNN architecture used here has been inspired by the work of Petrillo et al. (2017). The network architectures can be seen in Table 2. Robust initialization (HeNormal) is used to initialize the weights as this speeds up network convergence (He et al. 2015).

The networks have four convolutional layers initially, with $2 \times 2$ max-pooling incorporated twice after the first two convolutional layers. After the convolutional layers, the 2D feature maps that have been made in the final convolutional layer are flattened into a 1D vector to be used as input into the dense layer of fully connected neurons. The final layer is a classification layer, where the network gives each image a classification between 0 and 1. This number can be seen as a probability that the image is a lens. The CNN is trained on a set of 75 per cent of the labelled images from the data set, using a process of batch training with a batch size of 500. Five per cent of the data set is used for data validation to avoid overtraining. Throughout our networks we used ReLU [Rectified Linear Units (Nair & Hinton 2010)] for the activation functions and binary cross-entropy was used as the loss function.

5 RESULTS AND DISCUSSION

An image is judged to contain a lens if the classification from the network is above or equal to 0.5, conversely if the classification is below 0.5 the image is judged to not contain a lens. This value can be increased to give a more accurate classification, causing the number of false positives to decrease. However, it also means that more lenses are misclassified. 20 per cent of each data set is passed through the appropriate network to be classified; this is the test set. The scores for each network can be seen in Table 3. By looking at the percentage of images classified correctly, and the percentage of lenses and non-lenses classified correctly, the KiDS-like networks are more successful than the *Euclid* VIS-like networks. This is not surprising since the KiDS-like images have four image bands compared to the single band of the *Euclid* VIS-like images. This would imply that colour information from the multiple bands of the KiDS-like images has been helpful in classifying the lenses correctly, as one would expect as it helps greatly when classifying by eye. A test of this (which we will conduct in future work) would

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https://keras.io/
Table 1. Table describing the contents of each data set.

| Type                                | Description                                               | Number of lenses |
|-------------------------------------|-----------------------------------------------------------|-----------------|
| Euclid VIS-like simulations         | 100 000 single-band 1 × 101 × 101 simulated images         | 39 975          |
| KiDS-like simulations               | 100 000 multi-band 4 × 101 × 101 simulated images          | 49 862          |
| Euclid VIS-like simulations with COSMOS distribution | 68 923 single-band 1 × 101 × 101 simulated images | 24 029          |
| KiDS-like simulations with COSMOS distribution | 60 144 multi-band 4 × 101 × 101 simulated images | 29 960          |
| COSMOS lenses                       | 65 single-band real lenses cropped to 101 × 101 images     | 65              |

Table 2. Shows the architecture of the four networks: Euclid VIS-like and KiDS-like. What each layers contains, as well as each layers initial weights and biases. The final sigmoid layer gives an output between 0 and 1. For the convolutional and max-pooling layers, a stride length of 2 was used, meaning each pixel was only used once in pooling, padded with the same edge pixels where required.

| Type of layer | Layer contains | Initial weights | Initial bias |
|---------------|----------------|-----------------|--------------|
| Convolutional | 8 (15 × 15) image kernels | HeNormal | Zeros |
| Max-pooling   | Pooled over each (2 × 2) square | – | – |
| Convolutional | 8 (15 × 15) image kernels | HeNormal | Zeros |
| Max-pooling   | Pooled over each (2 × 2) square | – | – |
| Convolutional | 16 (5 × 5) image kernels | HeNormal | Zeros |
| Convolutional | 16 (5 × 5) image kernels | HeNormal | Zeros |
| Flatten       | Convert image maps into 1D vector | – | – |
| Dense         | 512 fully connected neurons | HeNormal | Zeros |
| Dense         | 1 sigmoid output neuron | HeNormal | Zeros |

Table 3. This table shows the percentage of images classified correctly, for lenses, non-lenses, and total correct.

| Images                                | Lenses correct (per cent) | Non-lenses correct (per cent) | Total correct (per cent) |
|---------------------------------------|---------------------------|-------------------------------|--------------------------|
| Euclid VIS-like simulations           | 60.32                     | 93.26                         | 80.13                    |
| KiDS-like simulations                 | 88.17                     | 86.82                         | 87.49                    |
| Euclid VIS-like simulations with COSMOS distribution | 56.14                     | 98.86                         | 93.33                    |
| KiDS-like simulations with COSMOS distribution | 76.83                     | 97.46                         | 93.62                    |

be to compare single-band KiDS-like images with multiband KiDS-like images. In both the COSMOS-like data sets, the percentage of lenses correctly identified is less than the original data sets. This is probably because the images with the largest rings (>4 arcsec Einstein radius) have been removed to make the data set. These images are easy to identify as lenses and so removing them decreases the success rate for lenses. However, non-lens classification success has increased with the same number of non-lens images involved. Although both the data sets have a similar overall success rate, the network trained on the Euclid VIS-like data set performed significantly worse at recognizing the images containing lenses. The difference in overall performance is most clear by looking at the receiver operating characteristic (ROC) curves for the data sets together in Fig. 6. A true positive is when a true image, one with a lens, is classified as such, while a false positive is when a false image, one without a lens, is classified as having a lens. The area under the ROC curve determines the results, 1 being the score for all classifications correct, 0 the score for all classifications incorrect, and 0.5 being the result of random selection. True negatives and false negatives are defined similarly. Fig. 6 confirms that the KiDS-like data set performed best, although the network only improved slightly using a subset of the images, unlike the Euclid data set that improved significantly by removing images from the data set.

As well as using simulated data, we tested on 65 real images from COSMOS. These are single-band images made from larger image cut-outs and modified to have the same PSF as the Euclid images by convolving with a suitable kernel. The full width at half maximum (FWHM) of Euclid squared is equal to the FWHM of COSMOS squared plus the FWHM of the kernel squared:

\[
\text{FWHM(Euclid)}^2 = \text{FWHM(COSMOS)}^2 + \text{FWHM(kernel)}^2.
\]

After convolution to match the Euclid PSF, the COSMOS images also had their pixels resampled to match the Euclid pixel scale. Images of the COSMOS lenses before and after applying the convolution can be seen in the Appendix. The resulting images were also 101 × 101 pixels. Having only 65 available images meant that training on these images was not a possibility, but testing them with the trained Euclid-like networks was. The results can be seen in Table 4. The scores for both networks were very low, and can be expected after training on a different type of image. Every COSMOS lens that has been classified incorrectly is a false negative. All of the images from the COSMOS survey can be seen in the Appendix. Nevertheless, our network recovers 16/31 of the lenses identifiable by eye at the Euclid resolution (see the Appendix), and 8/34 of the lenses that cannot be identified by eye. Although our network at Euclid resolution only recovers 20 per cent of the lenses known to exist at HST resolution, this is in itself quite interesting: it implies...
that the detectability of lensing is a very strong function of angular resolution. Roughly doubling the angular resolution (from *Euclid* to *HST* resolution) results in roughly a fivefold increase in the numbers of detectable lensing systems. Even though the KiDS-like subset showed a great deal of success, there are still things to be wary of: all the images used in this work in training and testing are simulated images, but real images may not be classified as accurately, which can be seen by looking at the results from the COSMOS images. The percentage of images containing a lens is much higher in these simulated cases than for the results from the COSMOS images. The percentage of images not be classified as accurately, which can be seen by looking at Table containing the classification results of the COSMOS lenses on two differently trained networks. Note all 65 images were lenses.

| Trained data set                  | Lenses correct |
|----------------------------------|----------------|
| *Euclid* VIS-like simulations    | 18 (27.69 per cent) |
| *Euclid* VIS-like simulations with COSMOS distribution | 15 (20.00 per cent) |

Figure 6. ROC curves for *Euclid* network (top) and KiDS network (bottom) with the area under the curve shown. The black dashed line indicates the curve for random choice.

Table 4.

6 CONCLUSIONS

A well-designed CNN can be used with future observations from *Euclid* and other similar surveys, as they are demonstrably successful on simulated data. Making more realistic simulations, more accurate distributions of Einstein radii and faint lens galaxies, will give a more accurate account of how CNNs will perform with real data. Machine learning techniques will provide a subset of ostensibly reliable lens systems, where verification by visual inspection can be achieved in a realistic time-scale that can then be used to refine the CNN.

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**APPENDIX: COSMOS LENSES**

The following figures show the 65 lenses from COSMOS that our CNNs were tested with. Each lens has the ID number below. Images with an asterisk after the ID number were the ones that were correctly identified as a lens. Each image has the usual North up, East left configuration, and are 10 × 10 arcsec. Images in the left column are from the COSMOS survey, in the right are the same images after being convolved with a kernel to give the image the same PSF as Euclid. The images have been grey-scale altered to best show the lens.

![Image](https://example.com/image.png)

**Figure A1.** Images of the COSMOS lenses before (left) and after (right) applying a convolution to match the Euclid PSF.
Figure A1 continued
Using CNNs to identify gravitational lenses

Figure A1 continued

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