Thermodynamic Study and Re-optimization of the Au-Ga Binary System

Dominika Jendrzejczyk-Handzlik

Submitted: 15 November 2016 / in revised form: 21 March 2017 / Published online: 5 April 2017
© The Author(s) 2017. This article is an open access publication

Abstract Activities of gallium in the liquid Au-Ga alloys were determined using galvanic cells with the solid oxide electrolyte. The cells of the type:

\[ \text{Au}_x\text{Ga}_{(1-x)}//\text{ZrO}_2+\text{Y}_2\text{O}_3//\text{Fe}, \text{FeO} \]

were used in the temperature range from 1050 to 1273 K, and for four alloy compositions \( x_{\text{Ga}} = 0.2, 0.4, 0.6 \) and 0.8. From the measured e.m.f.'s the activity of gallium was derived, which taken together with the recently measured heat of mixing provided precise description of the thermodynamic properties of the liquid phase. This study was supplemented with DTA experiments which were performed for three alloy compositions, namely 0.15, 0.25 and 0.40 gallium mole fraction. The results of these experiments verified with temperature of respective invariant reactions. Finally, present results, taken together with the information existing in the literature, were used for the calculation of the optimized Au-Ga phase diagram. ThermoCalc software was applied to complete these calculations.

Keywords E.M.F. measurements · DTA method · Au-Ga phase diagram

1 Introduction

The best known application of gold is in jewelry. A large variety of hand-made gold goods has been known since the ancient times. Recently, to push up the price of gold items, different colors of gold were introduced by addition of various alloying elements.\(^{[1-6]}\) Special colors of gold like purple, blue, or brown can be obtained using alloys of indium, gallium and aluminum.\(^{[7,8]}\)

However, thanks to its high electrical conductivity and anticorrosion properties, gold has been also used in interconnections applied in modern electronics industry. In order to develop the improved contact materials and to adjust temperature of the solders, multicomponent alloys can be applied in which gallium can be one of the possible metallic solutes. Gallium has excellent wetting properties and decreases the temperature of melting.\(^{[9]}\) Used as a solder alloy, the Cu-Ga system is a part of Cu-In-Ga-Se photovoltaics\(^{[10]}\) and Cu-Ga-N semiconductor systems.\(^{[11]}\) Kuznetsov and Shmelev\(^{[12]}\) investigated the influence of small gallium additions to gold and the interaction of Au-Ga alloys with silicon. They found that the increase of gallium concentration in the alloy results in the increase of stress in silicon. They also reported two isopleths determined for this ternary diagram containing 2.78 and 9.3 atomic percent of gallium. Gomidzelovic et al.\(^{[13]}\) investigated ternary Au-Ga-Sb system. Since Ga-Sb alloy belongs to the Group of III-V semiconductors, this study was to answer the question of the stability of contacts between Au and GaSb phase. The authors of this paper used thermodynamic calculations to determine thermodynamic properties of the liquid ternary system and demonstrated that the activity of gold as well as gallium exhibit negative deviation from the Raoult’s law. Recently, Manasijevic

---

1 Faculty of Non-Ferrous Metals, AGH University of Science and Technology, 30 Mickiewicza Avenue, 30-059 Kraków, Poland
et al.\cite{14} reported the results of thermal analysis and suggested phase equilibria in the ternary Au-Ga-Sb system.

Solid phase equilibria were analyzed in the ternary Au-Ga-As, Au-Ga-Sb systems by Thomas and Williams.\cite{15} The main objective of this work was to determine which metallic phases exist in equilibrium with the III-V semiconductors. Very recently, thermodynamic assessment of the ternary Au-In-Ga system was performed by Ghasemi et al.\cite{16} This system is useful in the growth of Au-seeded conductors. Very recently, thermodynamic assessment of metallic phases exist in equilibrium with the III-V semiconductor heterostructure and for that reason attracted more attention.

However, it seems that alloys containing gallium may find more interesting applications reaching beyond micro-electronic circuits. Mouani et al.\cite{17} studied Au-Ga-Te system because germanium and tellurium alloys exhibit interesting optical properties. Moreover, it was found recently that gallium containing multicomponent alloys can be used in dentistry.\cite{18} Thus, it seems that more and more multicomponent systems of interest contain gallium as a component.

Taking into account this wide spectrum of gallium alloys applications it seems to be reasonable to gather a reliable thermodynamic description of the binary systems that allows easy prediction of higher ordered alloys. Consequently, before starting to consider multicomponent gold alloys, respective binary systems with this element should be thoroughly described. Since gallium can be used as one component, there is also a need to create thermodynamic database of binary gallium alloys which can contribute to multicomponent systems. Consequently, we analyzed recently silver-gallium\cite{19} and copper-gallium\cite{20} binary alloys. As far as the Au-Ga binary system is concerned, it was already optimized twice, but under different assumptions. The first assessment was performed in 2010 by Liu et al.\cite{21} who took into account the nonstoichiometry of $\beta$ and $\gamma$ phases, but assumed the heat of mixing of liquid alloys to be temperature independent. In 2011 the next assessment was published by Wang et al.\cite{22} who treated all intermetallic phases existing in this system as line compounds. However, in their work, they assumed that the enthalpy of mixing is temperature dependent. Both papers showed good reproduction of the experimentally determined phase diagram. To gain more insight into the properties of this particular binary system, gold-gallium binary system has been re-investigated and next optimized in this work.

## 2 Literature Review

The binary gold-gallium system includes eight phases: FCC$_{\text{A1}}$, D0$_{24}$, $\beta$-Au$_3$Ga$_2$, $\beta$'-Au$_5$Ga$_2$, $\gamma$-Au$_7$Ga$_3$, AuGa, AuGa$_2$ and Liquid.

### 2.1 Thermodynamic Data

The enthalpy of mixing of this liquid binary system was measured by using different types of calorimeters. Using an adiabatic calorimeter Itagaki and Yazawa\cite{23} measured the enthalpy of mixing at 1373 K in the whole composition range of gallium. Predel and Stein\cite{24} determined the enthalpy of mixing in this liquid system by using a high-temperature calorimeter at 1423 K in the composition range from 0.0985 to 0.9 $x_{\text{Ga}}$. Gather and Blachnik\cite{25} reported the enthalpy of mixing at 1010 K, which was measured by the heat flow calorimeter in the composition range from 0.551 to 0.923 $x_{\text{Ga}}$. Using reaction calorimeter Bergman et al.\cite{26} measured the enthalpy of mixing in this binary system at 830 and at 1030 K in the composition range from 0.15 to 0.95 $x_{\text{Ga}}$. The enthalpy of mixing of liquid gold-gallium alloys at several different temperatures: 774, 787, 929, 1081, 1468, 1558 and 1661 K in the composition range from 0.30 to 0.94 $x_{\text{Ga}}$ was determined by Hayer et al.\cite{27} using reaction calorimetry. Beja\cite{28} measured $\Delta_{\text{mix}}H$ at 850 and at 1030 K in the composition range from 0.1 to 0.8 $x_{\text{Ga}}$.

Recently, Jendrezyczk-Handzik\cite{29} measured the enthalpies of mixing for the liquid Au-Ga system at two temperatures 1223 and 1323 K, in the composition range from 0.97 to 0.356 $x_{\text{Ga}}$ using high-temperature drop calorimeter.

All experimental results obtained from the calorimetric method show negative values of the enthalpy of mixing in the liquid phase. The experimental data\cite{25-29} are compatible with one another. Experimental values reported by Itagaki and Yazawa\cite{23} and Predel and Stein\cite{24} are less negative than the values reported in studies\cite{25-29} and these data were not used in the present optimization of binary gold-gallium system.

As far as the solid phases are concerned, Bergman et al.\cite{26} determined the enthalpy of formation of AuGa and AuGa$_2$ at 298 K using calorimetry method. Predel and Stein\cite{30} investigated the enthalpies of formation of AuGa and AuGa$_2$ phases at 700 K, by using liquid tin solution calorimetry. Predel and Stein\cite{24} determined the enthalpy of formation of fcc(Au) phase at 703 K over the range of compositions 0.03-0.10 at.% Ga. Wallbrecht et al.\cite{31} measured the enthalpy increments $(H_T^e - H_{298.15}^e)$ and heat capacity of three compounds: $\gamma$-Au$_5$Ga$_3$ at the composition Au$_{0.692}$Ga$_{0.308}$, AuGa at the composition Au$_{0.5}$Ga$_{0.5}$ and AuGa$_2$ at the composition Au$_{0.34}$Ga$_{0.66}$. Measurements were carried out using differential scanning calorimetry in the temperature range between 235 and 700 K. The values of the enthalpies formation of AuGa and AuGa$_2$ reported by Bergman et al.\cite{26} are more positive than those reported by Predel and Stein\cite{30} (the difference between them is
about 2000 J/mol). The experimental data from Refs 26, 30, and 31 were taken into account in the present optimization.

The activities of Au and Ga in liquid gold-gallium system were measured at 1400 K by Bergman et al. [26] who used Knudsen cell coupled with the mass spectrometer. Kameda and Azakami [32] determined the activity of gallium in liquid Au-Ga system at 973 and 1073 K using e.m.f. method with liquid salt electrolyte. Predel and Schallner [33] determined the excess Gibbs energy at 1000 K in liquid Au-Ga system in the range composition from 0.2 to 0.9 at. % Ga. This experimental data were taken into account in present optimization.

Experimental values of the activity of gallium at 973 and 1073 K determined by Kameda and Azakami [32] show much more negative deviation from Raoult’s law than the data of Bergman et al. [26]. Moreover, the activities of Ga in the liquid Au-Ga alloys reported in Ref 32 are independent of temperature. Due to possible exchange reaction between the alloy and molten salts, the data of Kameda and Azakami [32] were not used in the present optimization.

2.2 Phase Diagram Data

The Au-Ga system was studied first time by Weibke and Hesse [34] who used x-ray, microscopic and differential thermal analysis. Next, Owen and Roberts [35] determined the solubility of Ga in the fcc(Au) phase through the lattice parameter measurements, and consequently modified the solid solubility value of gallium in fcc(Au) given by Weibke and Hesse [34]. The solubility of Ga in the fcc(Au) phase was also reported by Kuznetsov and Shmelev [12] from the lattice parameter measurements and microscopic analysis in the low temperature range from 373 to 623 K. The most extensive study was conducted by Cooke and Hume-Rothery [36] who determined the liquidus, solidus and invariant reactions in this binary system in the whole composition range. The compositions and temperature of the invariant reactions were also given. The solubility of Ga in the fcc(Au) phase determined by Owen and Roberts [35] agrees well with the experimental data obtained by Kuznetsov and Shmelev [12] at low temperature but is slightly larger than that obtained by Cooke and Hume-Rothery [36] at high temperature (>700 K). Recently, using x-ray, microscopic and differential thermal analysis, Zivkovic et al. [37] determined the liquidus and invariant reactions in this system in the composition range from 0.6707 to \( x_{Ga} = 1 \). Temperatures of the liquidus reported in this paper are lower than those given in Weibke and Hesse [34] and Cooke and Hume-Rothery [36] works. No experimental data concerning the solubility of Au in orthorhombic (Ga) could be found in the published literature.

Solid intermetallic phases \( \beta'\)-Au7Ga2, \( \gamma\)-Au7Ga3, and \( \alpha\)-Au7Ga (D024) were detected and confirmed as having the hexagonal structure of Ni3Ti type (space group P63 mmc) by Cooke and Hume-Rothery [36,38]. The stability and composition of all intermetallic compounds have been examined carefully by Cooke and Hume-Rothery [36] who detected narrow homogeneity ranges of the intermetallic compounds \( \beta\)-Au7Ga2 (20.4-22.1 at. % Ga), \( \beta'\)-Au7Ga2 (21.3-23.2 at. % Ga), \( \gamma\)-Au7Ga3 and \( \gamma'\)-Au7Ga3 (29.8-31.0 at. % Ga). Solid phases AuGa, AuGa2, whose existence was also confirmed, exhibit almost stoichiometric composition. However, the results obtained by Cooke and Hume-Rothery [36] are different from those which were reported by Weibke and Hesse [34].

The structures of the stable intermetallic compounds: \( \alpha\)-Au7Ga, \( \beta\)-Au7Ga2, \( \beta'\)-Au7Ga2, \( \gamma\)-Au7Ga3, \( \gamma'\)-Au7Ga3, AuGa, AuGa2 were investigated experimentally by Frank [39], Wallace and Kitchin [40] and Puselj and Schubert [41]. Order-disorder transformation between \( \gamma\)-Au7Ga3 and \( \gamma'\)-Au7Ga3 was suggested by Cooke and Hume-Rothery [36]. Due to their narrow homogeneity ranges (29.8-31.0 at. % Ga) and unconfirmed order-disorder transition between \( \gamma\)-Au7Ga3 and \( \gamma'\)-Au7Ga3, this phase is modeled as one compound denoted as \( \gamma\)-Au7Ga3. The intermetallic compounds: AuGa and AuGa2 due to their almost fixed composition (limited solubility <2 at. %) can be considered as “line” compounds.

Experimental information mentioned above in Ref 34-41 was taken into account in the present optimization, while the solubility of Au in Orthorhombic (Ga) was neglected due to the lack of experimental information.

Au-Ga phase diagram was reviewed first time by Elliott and Shumk [42] but the phase boundary of the Au-rich terminal solid solution phase was uncertain. Next, Moffat [43] and Masalski and Okamoto [44] re-reviewed the Au-Ga phase diagram. Finally, Mouani et al. [17] re-investigated the Au-Ga phase diagram during their study of the Au-Ga-Te system. They reported temperature of the peritectic reaction \( L + fcc(Au) \rightarrow \alpha\)-Au7Ga2 to be 696 K. The temperature of this invariant reaction is different from the result of Cooke and Hume-Rothery [36] which is 688 K. Recently, Liu et al. [21] and Wang et al. [22] optimized Au-Ga phase diagram by means of CALPHAD (CALculation of PHase Diagrams) method.

3 Experimental

3.1 Materials

Gold rods of 5 mm in diameter were obtained from Men- nica Polska, Poland. Iron powders, metallic gallium, tungsten wire (diameter 0.5 mm) were obtained from Alfa Aesar, Germany. They were of minimum mass fractions purities 99.9999% (Au, Fe) and 99.99% (Ga, W).
Gallium(III) oxide and iron(IV) oxide with the minimum mass fraction purity 99.99% were obtained from Sigma Aldrich, Germany. The gas atmosphere was pure argon obtained from Air Products, of minimum mass fraction 99.999 used for the EMF method. Closed at one end YSZ electrolyte tubes (length 50 mm, outside diameter 8 mm) were supplied by the Yamari, Japan. Gold-gallium alloys were prepared from pure metals prior to EMF experiments. Similarly, weighed samples of about 200 mg prepared for DTA experiments with the following compositions: Au0.85Ga0.15, Au0.75Ga0.25 and Au0.60Ga0.40 were placed inside the thin quartz tubes, and then they were sealed under vacuum. Next, the samples were annealed in the operating furnace VMK22, Linn High Therm for 4 weeks at the temperature 473 K. After annealing they were transferred to DTA apparatus.

3.2 EMF Technique

A schematic representation of the cell assembly is shown and described in the previous papers.\textsuperscript{[19,20]} The working electrode was metallic alloy of a chosen composition with the addition of Ga2O3. The reference electrode was a mixture of Fe + FeO which was produced by heating the mixture of Fe and Fe2O3 powders under argon up to \( T = 1273 \) K. The cell was kept within the constant temperature zone of the furnace under a flow of purified argon. Initially, as electric lead wires tungsten wire was used. However, it was necessary to substitute it for the working electrode with kanthal wire with an attached iridium tip. The temperature inside the cell was maintained constant within \( \pm 1 \) K, which was achieved by using temperature controller Lumel type RE15. The EMF of the cell was recorded by means of the digital Keithley 2000 multimeter. Thanks to the program written in Delphi, EMF values were read out from the Keithley multimeter directly to the computer. Consequently, measurements were performed under very precise control of the EMF change with temperature. The measurements were carried out at increasing and decreasing temperature for three days.

3.3 DTA Measurements

DTA measurements were carried out on three Au-Ga alloys with the chosen composition \( x_{\text{Ga}} = 0.15, 0.25 \) and 0.40, and in the temperature range from 473 to 1300 K. The samples of the alloys were prepared from pieces of pure elements. The weight of samples used for the experiments was about 200 mg. The measurements were performed on DTA 404 apparatus from Netzsch, Selb, Germany. This device is hooked up to PC in order to control all DTA procedures during the experiment by PROTEUS software, also obtained from Netzsch. The acquired data were recorded on PC. The total experimental error of the method has been estimated to be \( \pm 1 \) K. Two different heating/cooling rates 5 and 2 K/min were used to verify the temperature of the detected phase transitions, starting from the annealing temperature up to about 323 K above the estimated liquidus temperature.

4 Results

4.1 E.M.F.’s Method

The gallium activity in Au-Ga system was determined by using EMF method with the cell (I) in the temperature range from 1050 to 1273 K.\textsuperscript{[19,20]} The spread of results reported in different studies is of the order of 30 kJ, which is about 3% of the measured value. On this basis, one can conclude that present results are in good agreement with those already published.

The overall reaction cell (I) is:

\[
3 \text{FeO} + 2 \text{Ga} = \text{Ga}_2\text{O}_3 + 3 \text{Fe}
\] (Eq 1)

For the reversible reaction (Eq 1), the change in Gibbs free energy can be derived as follows:

\[
\Delta_f G = -6FE = \Delta_f G_m^{\text{Ga}_2\text{O}_3} - 3 \Delta_f G_m^{\text{FeO}} - 2RT \ln a_{\text{Ga}}
\] (Eq 2)

If gallium is in its pure, liquid state \((a_{\text{Ga}} = 1.0)\) Eq 2 takes the form:

\[
-6FE_c = \Delta_f G_m^{\text{Ga}_2\text{O}_3} - 3 \Delta_f G_m^{\text{FeO}}
\] (Eq 3)

from which one can determine the change of Gibbs free energy of the reaction of formation of pure solid \( \text{Ga}_2\text{O}_3\):

\[
\Delta_f G_m^{\text{Ga}_2\text{O}_3} = -6FE_c + 3 \Delta_f G_m^{\text{FeO}}
\] (Eq 4)

Thus, from Eq 4 the Gibbs free energy of formation of the solid \( \text{Ga}_2\text{O}_3\), \( \Delta_f G_m^{\text{Ga}_2\text{O}_3} \) can be determined from \( E_c \) measured as a function of temperature against the Fe, FeO reference electrode.

The values of Gibbs free energy are described by the following temperature dependence:

\[
\Delta G_m^{\text{Ga}_2\text{O}_3} (\pm 4)/\text{kJ/mol} = -1049.02 + 0.2807 (T/K)
\] (Eq 5)

The data, given by Eq 5, were compared with the data already published in the literature.\textsuperscript{[19,20]} The spread between the results reported in different studies is of the order of 30 kJ, which is about 3% of the measured value. On this basis, one can conclude that present results are in good agreement with those already published.

E.m.f. values produced by the cell(I) and corrected for thermo-emf’s, are shown in Fig. 1. The resulting linear
equations obtained by the least square method, are presented in Table 1.

Next, by combining Eq 2 and 3 the following expression for the activity of gallium in the alloy with copper can be derived:

$$\ln a_{\text{Ga}} = \frac{3F}{RT} (E - E^\circ)$$

(Eq 6)

where $F$ is the Faraday constant, $T$ is the absolute temperature and $R$ is the gas constant.

Finally, from the measured EMF’s, the expression for the partial Gibbs free energy of gallium in the alloy can be easily derived:

$$\Delta \mu_{\text{Ga}} = RT \ln a_{\text{Ga}} = 3F(E - E^\circ) = 3F(\Delta a + \Delta b(T/K))$$

(Eq 7)

if the linear dependence of the type $a + bT$ is assumed for temperature variation of the EMF.

As an example, the activity of gallium in the Au-Ga alloys was calculated at 1273 and 1400 K and it is shown in Fig. 2 as a function of Ga mole fraction. These values are in good agreement with the results of Bergman et al. [26] who used high temperature Knudsen cell coupled with the mass spectrometer.

4.2 DTA Study

DTA curves recorded for three compositions $x_{\text{Ga}} = 0.15$, 0.25 and 0.40 are shown in Fig. 3 and 4. For compositions of alloys having mole fractions $x_{\text{Ga}} = 0.25$ and 0.4, the experiments were run with the rate 5 K/min and they showed clearly temperatures of invariant reactions and liquidus. For the sample with 0.15 mole fraction of gallium, the experiments were run with the rate 5 K/min to reveal temperature of liquidus and 2 K/min to better expose the temperature of invariant reactions. The obtained results of DTA analysis are gathered in Table 2.

### Table 1 The temperature dependence of the EMF of cell (I)

| $x_{\text{Ga}}$ | $\text{EMF}(T) = A + BT$ |
|-----------------|--------------------------|
| 1.00            | 0.486 -0.000207          |
| 0.80            | 0.470 -0.000203          |
| 0.60            | 0.427 -0.000205          |
| 0.40            | 0.325 -0.000169          |
| 0.20            | 0.186 -0.000147          |

5 Thermodynamic Modelling

5.1 Substitutional Solution: FCC_A1, D024, Orthorombic_Ga, Liquid

The substitutional solution model was assumed to be applicable to FCC_A1, D024, Orthorombic_Ga solid phases as well as to the liquid phase. The Gibbs free energy of pure elements with respect to temperature $^\circ G_i^\phi(T) = G_i^\phi(T) - H_i^{\text{SER}}(T) (298.15 \text{ K})$ for the element $i$ ($i = \text{Au, Ga}$) in $\phi$ ($\phi = \text{liquid, fcc, D024 and Ortorombic_Ga}$) is represented by Eq 8:

$$^\circ G_i^\phi(T) = a + bT + cT \ln b(T) + dT^2 + eT^{-1} + fT^3 + iT^4 + jT^7 + kT^{-9}$$

(Eq 8)

The $^\circ G_i^\phi(T)$ data are referred to the constant enthalpy value of the standard element reference $H_i^{\text{SER}}$ at 298.15 K and 1 bar as recommended by Scientific Group Thermodata Europe (SGTE). [45] The reference states are: FCC_A1 (Au), and Orthorombic_Ga (Ga). The $^\circ G_i^\phi(T)$ expression may be given for several temperature ranges, where the
Table 2  Summary of measured thermal effects

| Sample comp./x_{Ga} | Type reaction | Thermal analysis |
|---------------------|---------------|-----------------|
|                     |               | Heating/K        |
|                     |               | Invariant effects | Liquidus |
| 0.4                 | L → γ-Au_{Ga} + AuGa | 613 | 688 |
|                     | L → γ-Au_{Ga} + β'-Au_{Ga} | 620 | 661 |
|                     | L + β-Au_{Ga} → β'-Au_{Ga} | 647 | |
| 0.25                | β-Au_{Ga} → fcc(Au) + β'-Au_{Ga} | 581 | 1017 |
|                     | L + D024 ↔ β-Au_{Ga} | 684 | |
|                     | L + fcc(Au) ↔ D024 | 697 | |

Underlined: heating 5K/min
### Thermodynamic parameters of Au-Ga system

| Phase          | Thermodynamic parameters, J/mol | Ref |
|----------------|---------------------------------|-----|
| Au             |                                 |     |
| 298.15-929.4   | $G_{\text{HGSERAU}} = -6938.856 + 106.830098T - 22.754557 \ln(T)$ | Ref 45 |
|                | $-3.859247 \times 10^{-6}T^3 - 25097T - 25097T^{-1}$ |     |
| 929.4-1337.3   | $-93.586.481 + 1021.695437T - 155.7067449 \ln(T) + 87.56015 \times 10^{-3}T^2 - 11.518713 \times 10^{-6}T^3 + 1063721T^{-1}$ |     |
|                | $+314.067.829 - 2016.378254T + 263.2522592T \ln(T) - 118.216828 \times 10^{-3}T^2 + 8.923844 \times 10^{-6}T^3 - 67999832T^{-1}$ |     |
| 1337.3-1735.8  | $-12.133.783 + 165.272524T - 30.96167 \ln(T)$ |     |
| 1735.8-3200    |                                 |     |
| Ga             | $G_{\text{HGSERAU}} = +21.312.331 + 585.263691T - 108.2287832 \ln(T)$ | Ref 45 |
|                | $+227.155636 \times 10^{-3}T^2 - 118.575257 \times 10^{-6}T^3 + 439954T^{-1}$ |     |
| 302.9-4000     | $-7055.643 + 132.73019T - 26.0692906 \ln(T) + 0.1506 \times 10^{-3}T^2 - 0.040173 \times 10^{-6}T^3 - 118332T^{-1}$ |     |
| 200.0-302.9    | $G_{\text{HGSERAU}} = +5613.144 + 97.444232T - 22.754557 \ln(T)$ | Ref 45 |
|                | $-0.00385924T^3 + 3.79625 \times 10^{-7}T^3 - 25097T^{-1}$ |     |
| 929.4-1337.3   | $-81.034.481 + 1012.30956T - 155.706745 \ln(T)$ |     |
|                | $+0.08756015T^3 - 1.1518713 \times 10^{-3}T^3 + 1063721T^{-1}$ |     |
| 1337.3-1735.8  | $+326.619.829 - 2025.76412T + 263.252259T \ln(T)$ |     |
|                | $-0.118216828T + 8.923844 \times 10^{-6}T^3 - 67999832T^{-1}$ |     |
| 1735.8-3200    | $+418.217 + 155.886658T - 30.96167 \ln(T)$ |     |
| 200.0-302.9    | $C_{\text{HGSERAU}} = -15.821.033 \times 10^{-3}T^2 + 0.00385924T^3 - 3.79625 \times 10^{-7}T^3 - 25097T^{-1}$ |     |
|                | $+567.189697T - 108.228783 \ln(T) + 0.227155636T^2$ |     |
|                | $-1.18575257 \times 10^{-4}T^3 + 439954T^{-1} - 7.0171 \times 10^{-17}T^2$ |     |
| 302.9-4000.0   | $-1389.188 + 114.049043T - 26.0692906 \ln(T)$ |     |
|                | $+1.506 \times 10^{-3}T^2 - 4.0173 \times 10^{-6}T^3 - 118332T^{-1}$ |     |
| 200.0-302.9    | $C_{\text{HGSERAU}} = -64.836.418 - 1.6697 \ln(T)$ |     |
| 298.14-3200    | $L_{\text{HGSERAU}} = -26.517.288 + 8.315T$ |     |
| 200.0-302.91   | $L_{\text{HGSERAU}} = -12.480.212 + 14.248T$ |     |
| fcc(Au)        | $G_{\text{HGSERAU}} = +G_{\text{HGSERAU}}$ | Ref 45 |
| 200.0-302.91   | $G_{\text{HGSERAU}} = -17.512.331 + 575.063691T - 108.228783 \ln(T)$ |     |
|                | $+0.227155636T^2 - 1.18575257 \times 10^{-4}T^3 + 439954T^{-1}$ |     |
| 302.91-4000    | $-3255.643 + 122.53019T - 26.0692906 \ln(T)$ |     |
|                | $+1.506 \times 10^{-3}T^2 - 4.0173 \times 10^{-6}T^3 - 118332T^{-1} + 1.64547 \times 10^{37}T^{-9}$ |     |
| 200.0-302.9    | $C_{\text{HGSERAU}} = -39.175.271 - 9.9817T$ |     |
| 298.14-3200    | $C_{\text{HGSERAU}} = -942.717$ |     |
| Orthorombic (Ga) | $C_{\text{HGSERAU}} = +G_{\text{HGSERAU}} + 5000$ | Ref 45 |
| 200.0-302.91   | $C_{\text{HGSERAU}} = +G_{\text{HGSERAU}}$ | Ref 45 |
| D024           | $C_{\text{HGSERAU}} = +G_{\text{HGSERAU}} + 125 + 0.797T$ | Ref 48,49 |
| 200.0-302.91   | $C_{\text{HGSERAU}} = +G_{\text{HGSERAU}} + 4500 + 9.5T$ |     |
| 200.0-302.9    | $C_{\text{HGSERAU}} = -41.254.465 - 10.662T$ |     |
| 298.14-3200    | $C_{\text{HGSERAU}} = -14.732.616$ |     |
| $\beta$-Au$_2$Ga$_2$ | $G_{\text{HGSERAU}} = 0.78950 \times 10^{-5}G_{\text{HGSERAU}} + 0.21050 \times 10^{-5}G_{\text{HGSERAU}} - 10903.861 - 2.673T$ | This work |
| $\beta'$-Au$_2$Ga$_2$ | $G_{\text{HGSERAU}} = 0.77770 \times 10^{-5}G_{\text{HGSERAU}} + 0.22230 \times 10^{-5}G_{\text{HGSERAU}} - 12.318.231 - 1.276T$ | This work |
| $\gamma$-Au$_2$Ga$_2$ | $G_{\text{HGSERAU}} = 0.70 \times 10^{-5}G_{\text{HGSERAU}} + 0.30 \times 10^{-5}G_{\text{HGSERAU}} - 16.793.819 + 1.314T$ | This work |
| Au$_2$Ga$_2$   | $G_{\text{HGSERAU}} = 0.50 \times 10^{-5}G_{\text{HGSERAU}} + 0.50 \times 10^{-5}G_{\text{HGSERAU}} - 20.815.031 + 1.528T$ | This work |
| AuGa           | $G_{\text{HGSERAU}} = 0.3333 \times 10^{-5}G_{\text{HGSERAU}} + 0.6667 \times 10^{-5}G_{\text{HGSERAU}} - 21.839.222 + 0.778T$ | This work |
coefficients \(a, b, c, d, e, f, i, j, k\) have different values. The \(\phi G_i^\phi (T)\) functions are taken from SGTE Unary (Pure elements) TDB v.5.\(^{[45]}\) The Gibbs energy of the element \(i\), \(\phi G_i^\phi (T)\), in its SER state is denoted by \(G_{\text{HSER}}^i\), i.e. where \(i = (\text{Au, Ga})\). The GHSERAU and GHSERGA are Gibbs energies of gold and gallium in FCC_A1 and Orthorhombic_Ga structures, respectively.

The thermodynamic functions of pure elements are listed in Table 3. Solid and liquid solution phases are described by the substitutional solution model:\(^{[46]}\)

\[
G_m^\phi = x_{\text{Au}} G_{\text{Au}}^\phi (T) + x_{\text{Ga}} G_{\text{Ga}}^\phi (T) + RT \left( x_{\text{Au}} \ln x_{\text{Au}} + x_{\text{Ga}} \ln x_{\text{Ga}} + x_{\text{Au}} x_{\text{Ga}} \sum_j j L^\phi (x_{\text{Au}} - x_{\text{Ga}})^j \right) \tag{9}
\]

where \(x_{\text{Au}}\) and \(x_{\text{Ga}}\) are the mole fractions of Au and Ga, \(\phi\) is the phase (liquid, FCC_A1, D024, Orthorhombic_Ga) and \(j = 0, 1, 2\). The \(x_{\text{Au}} x_{\text{Ga}} \sum_j j L^\phi (x_{\text{Au}} - x_{\text{Ga}})^j\) term is the Redlich-Kister polynomial used to describe excess Gibbs free energy. Taking into account negligible solubility of gold in pure solid gallium, the phase Orthorhombic_Ga was treated as a pure element.

The molar Gibbs energy of the pure elements Au and Ga with the structure D024, \(G_{\text{Au}}^{\text{D024}} (T)\) and \(G_{\text{Ga}}^{\text{D024}} (T)\) is not given in the Scientific Group Thermodata Europe (SGTE) database.\(^{[45]}\) In the present work, because the crystal structure of the D024 phase is similar to the hexagonal close packed structure (hcp structure), \(G_{\text{Ga}}^{\text{D024}} (T)\) is assumed to be equal to, \(G_{\text{Ga}}^{\text{hcp}} (T)\) i.e. \(G_{\text{Ga}}^{\text{D024}} (T) = G_{\text{Ga}}^{\text{hcp}} (T) = +4500 - 9.5T\) J/mol. In turn, \(G_{\text{Au}}^{\text{D024}} (T)\) was reported by Liu et al.\(^{[48,49]}\) in the assessments of the Au-In and Au-In-Sn systems.

5.2 Intermetallic Compounds

In the Au-Ga binary system, five intermetallic compounds: \(\beta\)-Au\(_7\)Ga\(_2\), \(\beta'\)-Au\(_7\)Ga\(_2\), \(\gamma\)-Au\(_7\)Ga\(_3\), AuGa and AuGa\(_2\), are treated as stoichiometric compounds \((\text{Au}_{x}G_{a}y)\) because of their narrow homogeneity ranges as determined by Cooke and Hume-Rothery.\(^{[36]}\)

- AuGa has a structure of the MnP(B31)-type,\(^{[11,14,31]}\)
- AuGa\(_2\) has isotypic CaF\(_2\)(C1)-type structure,\(^{[38,41,50]}\)
- \(\beta\)-Au\(_7\)Ga\(_2\) has a hexagonal structure\(^{[39,41]}\) and extends from \(\sim 20.4\) to \(22.1\) at.\% Ga,\(^{[17,36]}\)
- \(\beta'\)-Au\(_7\)Ga\(_2\) is formed peritectically at 682.8 K and exists unchanged down to room temperature. It has an orthorhombic structure\(^{[36]}\) and has a homogeneity range between 21.3 and 24.8 at.\% Ga\(^{[17,36,44]}\)
- \(\gamma\)-Au\(_7\)Ga\(_3\) has orthorhombic structure.\(^{[36,44]}\)

All binary stoichiometric compounds \(\text{Au}_{x}G_{a}y\) were described as the line compounds using the following expression:
Table 4  Invariant reactions in the Au-Ga system

| Invariant reaction                                      | Type       | $T$, K | Ref            |
|--------------------------------------------------------|------------|--------|----------------|
| $L + \text{fcc}(\text{Au}) \leftrightarrow D024$       | Peritectic | 688    | Ref 36         |
|                                                        |            | 696    | Ref 17         |
|                                                        |            | 696    | Ref 21         |
|                                                        |            | 693    | Ref 22         |
|                                                        |            | 697    | This work-DTA method |
|                                                        |            | 690    | This work-calculated |
| $L + D024 \leftrightarrow \beta$-Au$_7$Ga$_2$          | Peritectic | 683    | Ref 36         |
|                                                        |            | 683    | Ref 17         |
|                                                        |            | 683    | Ref 21         |
|                                                        |            | 679    | Ref 22         |
|                                                        |            | 684    | This work-DTA method |
|                                                        |            | 678    | This work-calculated |
| $L + \beta$-Au$_7$Ga$_2 \leftrightarrow \beta'$-Au$_7$Ga$_2$ | Peritectic | 648    | Ref 36         |
|                                                        |            | 648    | Ref 21         |
|                                                        |            | 644    | Ref 22         |
|                                                        |            | 647    | This work-DTA method |
|                                                        |            | 648    | This work-calculated |
| $L \leftrightarrow \gamma$-Au$_7$Ga$_3 + \beta'$-Au$_7$Ga$_2$ | Eutectic  | 620    | Ref 36         |
|                                                        |            | 622    | Ref 21         |
|                                                        |            | 623    | Ref 22         |
|                                                        |            | 620    | This work-DTA method |
|                                                        |            | 621    | This work-calculated |
| $L \leftrightarrow \gamma$-Au$_7$Ga$_3$                 | Congruent  | 623    | Ref 36         |
|                                                        |            | 622    | Ref 21         |
|                                                        |            | 624    | Ref 22         |
|                                                        |            | 621    | This work-calculated |
| $L \leftrightarrow \gamma$-Au$_7$Ga$_3 + \text{AuGa}$   | Eutectic  | 613    | Ref 36         |
|                                                        |            | 619    | Ref 21         |
|                                                        |            | 619    | Ref 22         |
|                                                        |            | 613    | This work-DTA method |
|                                                        |            | 613    | This work-calculated |
| $L \leftrightarrow \text{AuGa}$                         | Congruent  | 735    | Ref 36         |
|                                                        |            | 735    | Ref 21         |
|                                                        |            | 732    | Ref 22         |
|                                                        |            | 734    | This work-calculated |
| $L \leftrightarrow \text{AuGa} + \text{AuGa}$           | Eutectic  | 722    | Ref 36         |
|                                                        |            | 727    | Ref 21         |
|                                                        |            | 726    | Ref 22         |
|                                                        |            | 724    | This work-calculated |
| $L \leftrightarrow \text{AuGa}_2$                       | Congruent  | 764    | Ref 36         |
|                                                        |            | 764    | Ref 21         |
|                                                        |            | 764    | Ref 22         |
|                                                        |            | 764    | This work-calculated |
| $L \leftrightarrow \text{AuGa}_2 + (\text{Ga})$         | Eutectic  | 303    | Ref 36         |
|                                                        |            | 303    | Ref 21         |
|                                                        |            | 303    | Ref 22         |
|                                                        |            | 303    | This work-calculated |
where a and b are ratios of steechiometry, the C and D are adjustable parameters to be optimized, T temperature and $\gamma G_{Au}^{fcc}$ and $\gamma G_{Ga}^{Ort}$ are Gibbs energies of elements in their reference state.

### 6 Optimization Procedure

The thermodynamic parameters for all phases existing in the binary system were optimized using ThermoCalc software.\cite{53} For this optimization, thermodynamic data for the liquid and solid phases, invariant reactions and liquidus/solidus were used, and optimization was done according to Schmid-Fetzer et al.\cite{52} guideline, similarly to previous works.\cite{19,20,53,54} Each piece of the selected information was given a certain weight based on experimental uncertainty. The optimization was carried out step by step. First, the optimization of the liquid phase was performed, and then the solid phases were assessed. All parameters were finally evaluated together to provide the best description of the system. The calculated interaction parameters are gathered and shown in Table 3.

### 7 Results and Discussion

The calculated Au-Ga phase diagram superimposed with experimental data obtained by Weibke and Hesse,\cite{34} Owen and Roberts,\cite{35} Cooke and Home-Rothery,\cite{36}
Kuznetsov and Shmelev\cite{12} is shown in Fig. 5. It is seen from this figure that calculated phase diagram is in very good agreement with the experimental data, except for several data points Weibke and Hesse\cite{34} in the Au-rich part and Zivkovic et al.\cite{37} in the Ga-rich part.

Based on the heating curves obtained in the present work from differential thermal analysis, temperature of liquidus and invariant reactions were determined for $x_{Ga} = 0.15, 0.25$ and $0.4$ mole fraction. The calculated and measured information about invariant reactions are gathered in Table 4. It is seen again, that the results obtained in the present work are in very good agreement with the literature data Ref 36 and the results of calculations.

Thermodynamic properties of the liquid Au-Ga solutions were determined in the present work using solid oxide galvanic cells in the temperature range from 1050 to 1273 K. The electrochemical cells with YSZ solid electrolyte worked reversibly for three days with no sign of any side reaction. Reproducibility of the cell performance was checked by running experiments in cooling and heating cycles. From time to time a small current was passed through the cell at constant temperature. The e.m.f. returned always to the initial value in several minutes. These tests confirmed reproducible cell operation and speak for the lack of side reactions. The activity of gallium at 1273 and 1400 K derived from e.m.f. values was used for the description of thermodynamic properties of the liquid solutions. The activities of gallium in liquid Au-Ga alloys, which are obtained in present work, show negative deviation from Raoult’s low which decreases with rising temperature.

Fig. 6 shows the calculated activity of gallium in the liquid Au-Ga alloys at 1273 and 1400 K obtained in present work together with the experimental data of Bergman et al.\cite{26} at 1400 K. The values of gallium activity obtained at $T = 1400$ K are in good agreement with Bergman at al.\cite{26} for $x_{Ga} = 0.8, 0.4$ and 0.2. The result of the $a_{Ga}$ obtained for $x_{Ga} = 0.6$ by Bergman et al.\cite{26} is slightly more positive. Calculated activity of gallium is in good agreement with the experimental results at 1273 and 1400 K.

The comparison of the enthalpies of mixing of the liquid Au-Ga alloys between calculated results and experimental values, which were obtained in the temperature range from 774 to 1660 K, are shown in Fig. 7. All experimental results obtained from the calorimetric method show negative values of the enthalpy of mixing in the liquid phase. The experimental data obtained by Gather and Blachnik,\cite{25} Bergman et al.\cite{26} Hayer et al.\cite{27} and Beja and Jendrzejczyk-Handzlik\cite{29} are compatible with one another. Experimental values reported by Itagaki and Yazawa\cite{23} and Predel and Stein\cite{24} are less negative than the values reported in Ref 25-29. In the literature Ref 21, 22 there are two different interpretations of this enthalpy temperature dependence. Liu et al.\cite{21} assumed temperature independent heat of mixing in this system. They used all available

\[ HMR \]

\[ MOLE\_FRACTION\_GA \]

\[ \triangle \] Hayer et al.\cite{27} 1661 K

\[ \square \] Bergman et al.\cite{26} 830 K

\[ \bigtriangleup \] Beja \cite{28} 850 K

\[ \blacktriangleleft \] Gather and Blachnik \cite{25} 1010 K

\[ \blacktriangledown \] Bergman et al.\cite{26} 1030 K

\[ \blacksquare \] Beja et al.\cite{28} 1050 K

\[ \blacklozenge \] Jendrzejczyk-Handzlik \cite{29} 1223 K

\[ \bigtriangledown \] Jendrzejczyk-Handzlik \cite{29} 1323 K

\[ \bigcirc \] Itagaki and Yazawa \cite{23} 1373 K

\[ \star \] Predel and Stein 1423 \cite{24} K

\[ \bigtriangleup \] Hayer et al.\cite{27} 1661 K

\[ \square \] Bergman et al.\cite{26} 830 K

\[ \bigtriangleup \] Beja \cite{28} 850 K

\[ \blacktriangleleft \] Gather and Blachnik \cite{25} 1010 K

\[ \blacktriangledown \] Bergman et al.\cite{26} 1030 K

\[ \blacksquare \] Beja et al.\cite{28} 1050 K

\[ \blacklozenge \] Jendrzejczyk-Handzlik \cite{29} 1223 K

\[ \bigtriangledown \] Jendrzejczyk-Handzlik \cite{29} 1323 K

\[ \bigcirc \] Itagaki and Yazawa \cite{23} 1373 K

\[ \star \] Predel and Stein 1423 \cite{24} K

\[ \bigtriangleup \] Hayer et al.\cite{27} 1661 K
experimental results in Ref 23-28 of the enthalpy of mixing in their optimization, and they reported reasonable agreement between the calculated results and the experimental data. In turn, Wang et al. [22] suggested a temperature dependence of the enthalpy of mixing in the liquid Au-Ga system. However, in their optimization, the experimental values reported by Itagaki and Yazawa [23] and Predel and Stein [24] were not taken into account. The calculated enthalpies of mixing of the liquid Au-Ga alloys are in good agreement with the experimental data Ref 25-28. In both papers Liu et al. [21] and Wang et al. [22] the substitutional solution model was used to describe liquid phase in this binary alloy. In the present work, the experimental values reported by Itagaki and Yazawa [23] and Predel and Stein [24] were not taken into account in optimization of the liquid phase in Au-Ga system. It was assumed that in the examined temperature range (from 774 to 1660 K), the enthalpy of mixing in this binary system does not exhibit temperature dependence. It is shown that under this assumption satisfactory agreement is obtained between the calculated values and the experimental data Ref 25-29.

The heat of formation calculated at 298 K for the solid alloys and intermetallic compounds AuGa and AuGa₂ is shown in Fig. 8. The calculated enthalpies of formation of solid alloys and intermetallic compounds are in good agreement with the experimental data Ref Predel and Stein [24] for fcc(Au) phase and Predel and Schalle [30] and Bergman et al. [26] for AuGa and AuGa₂ phases.

This result is similar to that obtained by Liu et al. [21]. However, further experimental investigations to measure the standard enthalpy of formation should be done.

Summarizing, a new set of thermodynamic parameters was proposed for thermodynamic description of the binary gold-gallium system. Calculations done by using this set of thermodynamic parameters reproduced experimental data well, thus the thermodynamic database can be used not only for the description of the binary system but also as part of the description of higher-ordered systems.

Acknowledgments This work realized at AGH University of Science and Technology, Faculty of Non-Ferrous Metals under Grant Number IP2011020471 was supported by the Ministry of Science and Education.

Open Access This article is distributed under the terms of the Creative Commons Attribution 4.0 International License (http://creativecommons.org/licenses/by/4.0/), which permits unrestricted use, distribution, and reproduction in any medium, provided you give appropriate credit to the original author(s) and the source, provide a link to the Creative Commons license, and indicate if changes were made.

References

1. C. Cretu and E. van der Lingen, Coloured Gold Alloy, Gold Bull., 1999, 32, p 115–126
2. C.W. Corti, Blue, Black and Purple. The Special Colours of Gold, The Santa Fe Symposium, E. Bell, Ed., Met-Chem Research, Albuquerque, 2004, p 121–133
48. H.S. Liu, Y. Cui, K. Ishida, and Z.P. Jin, Thermodynamic Reassessment of the Au-In Binary System, *Calphad*, 2003, 27, p 27–37
49. H.S. Liu, C.L. Liu, K. Ishida, and Z.P. Jin, Thermodynamic Modeling of the Au-In-Sn System, *J. Electron. Mater.*, 2003, 32, p 1290–1296
50. H. Pfisterer and K. Schubert, New Phases of MnP(B31) Type, Z. *Metallkd.*, 1950, 41, p 358–367
51. ThermoCalc v., *Foundation Computational Thermodynamic*, Stockholm, Sweden, 2015, p 2014
52. R. Schmid-Fetzer, D. Andersson, P.Y. Chevalier, L. Eleno, O. Fabrichnaya, U.R. Kattner, B. Sundman, C. Wang, A. Watson, L. Zabdyr, and M. Zinkevich, Assessment Techniques, Database Design and Software Facilities for Thermodynamics and Diffusion, *Calphad*, 2007, 2007(31), p 38–52
53. W. Gierlotka, J. Łapsa, and D. Jendrzejczyk-Handzlik, Thermodynamic Description of the Pb-Te System Using Ionic Liquid Model, *J. Alloys Compd.*, 2009, 479, p 152–156
54. W. Gierlotka, D. Jendrzejczyk-Handzlik, P. Handzlik, and K. Fitzner, On the Ternary Ag-Cu-Ga System: Electromotive Force Measurement and Thermodynamic Modeling, *J. Alloys Compd.*, 2015, 646, p 1023–1031