A variable P\textsuperscript{v} broad absorption line and quasar outflow energetics

D. M. Capellupo,\textsuperscript{1,2} F. Hamann\textsuperscript{1} and T. A. Barlow\textsuperscript{3}

\textsuperscript{1}Department of Astronomy, University of Florida, Gainesville, FL 32611-2055, USA
\textsuperscript{2}School of Physics and Astronomy, Tel Aviv University, Tel Aviv 69978, Israel
\textsuperscript{3}Infrared Processing and Analysis Center, California Institute of Technology, Pasadena, CA 91125, USA

Accepted 2014 July 23. Received 2014 July 23; in original form 2014 May 9

ABSTRACT

Broad absorption lines (BALs) in quasar spectra identify high-velocity outflows that might exist in all quasars and could play a major role in feedback to galaxy evolution. The viability of BAL outflows as a feedback mechanism depends on their kinetic energies, as derived from the outflow velocities, column densities, and distances from the central quasar. We estimate these quantities for the quasar, Q1413+1143 (redshift $z_e = 2.56$), aided by the first detection of $P\nu\lambda\lambda 1118, 1128$ BAL variability in a quasar. In particular, $P\nu$ absorption at velocities where the $C\ IV$ trough does not reach zero intensity implies that the $C\ IV$ BAL is saturated and the absorber only partially covers the background continuum source (with characteristic size $< 0.01$ pc). With the assumption of solar abundances, we estimate that the total column density in the BAL outflow is $log N_H \gtrsim 22.3$ cm\textsuperscript{-2}. Variability in the $P\nu$ and saturated $C\ IV$ BALs strongly disfavours changes in the ionization as the cause of the BAL variability, but supports models with high column density BAL clouds moving across our lines of sight. The observed variability time of 1.6 yr in the quasar rest frame indicates crossing speeds $> 750$ km s\textsuperscript{-1} and a radial distance from the central black hole of $\lesssim 3.5$ pc, if the crossing speeds are Keplerian. The total outflow mass is $\sim 4100$ M\odot, the kinetic energy $\sim 4 \times 10^{54}$ erg, and the ratio of the outflow kinetic energy luminosity to the quasar bolometric luminosity is $\sim 0.02$ (at the minimum column density and maximum distance), which might be sufficient for important feedback to the quasar’s host galaxy.

Key words: galaxies: active – quasars: absorption lines – quasars: general.

1 INTRODUCTION

Broad absorption lines (BALs) in quasar spectra identify high-velocity outflows that originate from the quasar accretion disc and could play a major role in feedback to galaxy evolution. In order to determine the viability of BAL outflows as a feedback mechanism, we need estimates of their mass outflow rates and kinetic energy yields. These quantities depend on the outflow speeds, which are easy to measure, plus the column densities and distances of the flows from the central super massive black holes (SMBH), which are much more difficult to derive. Distances can be inferred in some cases from BAL variability (Misawa et al. 2007; Moe et al. 2009; Capellupo et al. 2011, 2013; Hall et al. 2011; Rodríguez Hidalgo, Hamann & Hall 2011; Rodríguez Hidalgo et al. 2013) or from excited-state lines with photoionization modelling (Moe et al. 2009; Dunn et al. 2010; Borguet et al. 2013). Column density estimates are hampered by saturation. In an unknown number of cases, the apparent optical depths of BAL troughs give just lower limits on the true optical depths and column densities because the absorbing gas only partially covers the background light source (e.g. Hamann 1998; Arav et al. 1999; Gabel et al. 2003).

One way to overcome the problem of saturation in BALs is to search for absorption in low-abundance ions, such as $P\nu$ (P/C $\sim 0.001$ in the Sun; Asplund et al. 2009). $P\nu$ is a good choice because it has a resonance doublet at accessible wavelengths, 1118 and 1128 Å, and its ionization is similar to much more abundant and commonly measured ions such as $C\ IV\lambda\lambda 1548,1551$. $P\nu$ absorption should be present if the column densities in the outflows are large enough. Originally, detections of $P\nu$ absorption were interpreted as indications of a vast overabundance of phosphorus (e.g. Turnshek 1988; Junkkarinen et al. 1997; Hamann 1998). The main problem is a poor understanding of the true BAL optical depths due to partial covering of the background continuum source (Hamann 1998; Arav et al. 1999; Hamann et al. 2002; Gabel et al. 2003). However, if the relative abundances are roughly solar, the presence of $P\nu$ absorption implies that $C\ IV$ and other common BALs are extremely optically thick and the total outflow column densities are much larger than previously supposed. For example, assuming solar abundances and a standard ionizing spectrum in photoionization models, Hamann (1998) showed that the true $C\ IV$...
optical depths in one BAL quasar are at least $\sim$800 times greater than P\,\textsc{v} in idealized BAL clouds that are optically thin throughout the Lyman continuum. In other situations with total column densities up to $N_H \sim 4 \times 10^{23}$ cm$^{-2}$, the ratio of C\,\textsc{iv} to P\,\textsc{v} optical depths might be as low as $\sim$100. Leighly et al. (2009) and Leighly, Dietrich & Barber (2011) present similar results across a wide range of physical conditions. Using many more observational constraints on the outflow conditions in a particular quasar, Borguet et al. (2012) estimated that the C\,\textsc{iv}/P\,\textsc{v} optical depth ratio should be $\sim$1200. Altogether these results show that even a weak P\,\textsc{v} detection indicates a very saturated C\,\textsc{iv} BAL and large total column densities.

As part of our survey to study BAL variability (Capellupo et al. 2011, 2012, 2013), we discovered variability in P\,\textsc{v} and other BALs in the quasar Q1413+1143. The P\,\textsc{v} absorption was detected previously by Monier, Turnshek & Lupie (1998). However, this is the first report of P\,\textsc{v} BAL variability, in this or any quasar, to our knowledge. It is significant because it confirms that the measured feature is indeed P\,\textsc{v} in the quasar’s BAL outflow rather than a coincidental broad blend of unrelated, intervening Ly$\alpha$ absorption lines in the Ly$\alpha$ forest. It is also significant because it favours models for the variability that involve clouds crossing the line of sight at high speeds (Hamann et al. 2008; Hall et al. 2011; Capellupo et al. 2012, 2013; Wildy, Goad & Allen 2014). We analyse new and existing spectra of Q1413+1143 to derive new constraints on the location and column densities of the BAL outflow.

Q1413+1143, also known as the Cloverleaf, is a well-studied lensed quasar at $z_s = 2.563$ (Adelman-McCarthy et al. 2008), with four components of similar brightness. The faintest component is within 0.5 mag of the brightest component (Turnshek et al. 1997). The components have a small separation: all are within 0.6 arcsec of the image centre (Magain et al. 1988). The four components are also similar spectroscopically. Although the BEL equivalent widths are smaller, and there are some small differences in the C\,\textsc{iv} absorption profile, in the faintest component (Angonin et al. 1990), Hutsemékers et al. (2010) attribute the spectral differences in this faint component to a long-term microlensing effect, which magnifies the continuum source in this component.

Section 2 describes the data and properties of Q1413+1143. Section 3 discusses the variability in the P\,\textsc{v} BAL and describes the constraints that the P\,\textsc{v} detection places on the column density of the outflow in this quasar. Section 4 discusses our estimates of the energetics of this flow and their implications.

## 2 DATA

During the BAL monitoring campaign described in Capellupo et al. (2011, 2012, 2013), we monitored 24 BAL quasars, including Q1413+1143, and we searched for variability in the C\,\textsc{iv} and Si\,\textsc{iv} absorption lines. In Q1413+1143, we also detected a variable P\,\textsc{v} absorption line. The monitoring campaign includes seven epochs of ground-based data for this quasar, but only three have wavelength coverage that extends blue enough to include the P\,\textsc{v} BAL. The first of these three spectra is originally from Barlow (1993), observed in 1989 April, and the second spectrum is from the Sloan Digital Sky Survey (SDSS; Adelman-McCarthy et al. 2008) and was taken in 2006 April. The most recent spectrum was taken in 2011 February at the KPNO 2.1 m. As mentioned earlier, Q1413+1143 is lensed. However, given the small separation between the four components, these spectra include light from all four components.

We further supplement our data set for Q1413+1143 with spectra from the Hubble Space Telescope (HST) archive. Q1413+1143 was observed by both faint object spectrograph (FOS) and space telescope imaging spectrograph (STIS). The FOS data have individual observations of each of the four lens components. We use the sum of the four components to compare to the observations above that include integrated light from all the components. We note that the D component of the lens had a weaker Ly$\alpha$ 1216 emission line than the other components (see also Angonin et al. 1990), but the absorption in P\,\textsc{v} is identical in all the components. For the STIS data, there are separate observations of just the A and B components of the lens. The two spectra are nearly identical, so we combined them to improve the signal to noise.

Table 1 summarizes all of the data covering P\,\textsc{v} that we discuss in this paper. The first column gives the fractional years of each observation. The next three columns list the observatories, the spectral resolution of the data, and the wavelength coverage. The final column lists the rest-frame time-scale, $\Delta t$, in comparison to the first observation, from 1989.26. For more details on these data, see Capellupo et al. (2011) for the Lick and SDSS spectra, Monier et al. (1998) for the HST FOS spectra, Monier, Turnshek & Rao (2009) for the HST STIS spectra, and Capellupo et al. (2013) for the KPNO spectrum.

For some of our discussion of the BAL outflow properties below, we estimate a bolometric luminosity based on $L_{bol}$ (1500 Å), measured from the absolute flux-calibrated Lick spectrum, in a cosmology with $H_0 = 71$ km s$^{-1}$ Mpc, $\Omega_M = 0.3$, and $\Omega_\Lambda = 0.7$. Using a standard bolometric correction factor, $L \approx 4.43 L_{bol}$ (1500 Å) (Hamann et al. 2011), and dividing by a lens magnification factor of 11 (Venturi & Solomon 2003) gives a bolometric luminosity of $L = 2.4 \times 10^8$ erg s$^{-1}$ for Q1413+1143. We approximate the black hole mass by assuming $L = 1/3 L_{bol}$, which gives $M_{\bullet} \approx 4.8 \times 10^9 M_\odot$.}

## 3 ANALYSIS AND RESULTS

### 3.1 Variability in a P\,\textsc{v} absorption line

In the variability study described in Capellupo et al. (2011, 2012), we find that Q1413+1143 varied in both C\,\textsc{iv} and Si\,\textsc{iv}. We also detect the P\,\textsc{v} absorption line with variability at velocities corresponding to the variability in both C\,\textsc{iv} and Si\,\textsc{iv}, which we discuss here for the first time. Out of the seven epochs of data we have for this object in our BAL monitoring programme, three of the spectra extend blue enough to show this P\,\textsc{v} absorption (Table 1).

We adopt the Lick spectrum here as the fiducial spectrum, for which we fit a pseudo-continuum in Capellupo et al. (2011). We use the same pseudo-continuum fit in this paper. This pseudo-continuum includes a power-law fit to the continuum in regions free of emission and absorption, and for Q1413+1143, we used the spectral regions at 1270$-$1290 and 1680$-$1700 Å. We also fit multiple Gaussians to the C\,\textsc{iv} and Si\,\textsc{iv} broad-emission lines (BELs) to get a smooth fit to the profiles. The Si\,\textsc{iv} and C\,\textsc{iv} BELs were fitted in Capellupo et al. (2011) in order to properly measure the Si\,\textsc{iv} and C\,\textsc{iv} BALs. We
do not fit the Lyα, N \textsc{v}, or O \textsc{vi} BALs or adjacent emission lines in the Lyα forest because of the large uncertainties and, specifically, the severe blending of Lyα and N \textsc{v} with each other and possibly with Si \textsc{iii} λ1206. Also, the O \textsc{vi} BAL is not covered in the Lick 1989.26 spectrum and, therefore, it is not useful for our variability analysis. While we do measure the P \textsc{v} absorption, we do not fit P \textsc{v} emission because it does not have a significant emission line.

The black dotted curve in Fig. 1 shows the pseudo-continuum fit, combining the power-law continuum fit and the fits to the Si \textsc{iv} and C \textsc{iv} BELs.

The strongest BALs in our data are identified by horizontal solid lines in Fig. 1. Redward of the Lyα emission are the well-studied, aforementioned Si \textsc{iv} and C \textsc{iv} BALs. Blueward of Lyα are O \textsc{vi} λ1037, Si \textsc{iv} λλ1063,1073, P \textsc{v}, and N \textsc{v} λλ1239,1243 (Leighly et al. 2009; Baskin, Laor & Hamann 2013).

To compare the spectra from different epochs, we use a simple multiplicative shift, with no change to the slope, to match the spectra along regions free of emission and absorption. Fig. 1 shows the Lick spectrum from 1989.26 (black curve), with the HST FOS (1994.98; purple curve), HST STIS (2000.29; green curve), SDSS (2006.31; red curve), and KPNO (2010.11; blue curve) spectra overplotted. The C \textsc{iv} BAL has a longer wing on the blue side of the profile in the Lick spectrum, and the variability in the BAL extends to higher outflow velocities than in Si \textsc{iv}. There also appears to be variability in N \textsc{v} at ~1140–1160 Å, corresponding to the variability in the wing of the C \textsc{iv} line. We do not have coverage across O \textsc{vi} in the Lick spectrum, so we cannot compare its variability properties to those of the other lines. We also note that there is variability between the Lick spectrum and the later spectra at ~1580 Å, which may be caused by variability in Fe \textsc{ii} emission lines and/or absorption in these features (Vestergaard & Peterson 2005).

To compare the variability in the different lines, we mark the region of variability in the blue side of the Si \textsc{iv} trough with a shaded bar. We then mark the corresponding velocities in the P \textsc{v}, N \textsc{v}, and C \textsc{iv} BALs with shaded bars, with the widths of the bars adjusted for the different doublet separations in the lines. C \textsc{iv} has the narrowest doublet separation at 498 km s\(^{-1}\), and Si \textsc{iv} and P \textsc{v} have wider doublet separations of 1930 and 2670 km s\(^{-1}\), respectively.

Fig. 2 shows the C \textsc{iv}, Si \textsc{iv}, and P \textsc{v} profiles for three of the epochs, namely, Lick 1989.26, SDSS 2006.31, and KPNO 2010.11, shown here again with black, red, and blue curves, respectively. We plot here the normalized spectra, after dividing by the pseudo-continuum fit shown in Fig. 1. The velocity scales in the three panels are defined based on the wavelength of the short-wavelength doublet member for each ion.

Fig. 2 shows clearly how the profiles of these three lines match in velocity space. The main difference, as mentioned above, is that C \textsc{iv} has a more extended wing on the blue side of the profile and the variability extends to higher outflow velocities than in Si \textsc{iv} and P \textsc{v}. The velocities where variability occurred in the blue side of the Si \textsc{iv} trough and in the P \textsc{v} trough closely match. The P \textsc{v} line also varies in the same sense as C \textsc{iv} and Si \textsc{iv}; all of the lines get

\begin{figure*}[ht]
\centering
\includegraphics[width=\textwidth]{spectra.png}
\caption{Spectrum of Q1413+1143, showing all of the epochs outlined in Section 2 and Table 1. The middle shaded region marks the interval of variability in Si \textsc{iv} in the blue side of the trough, and, in order of increasing wavelength, the other three shaded regions show the corresponding velocity intervals in P \textsc{v}, N \textsc{v}, and C \textsc{iv}. The black dotted curve is the pseudo-continuum fit, and formal 1σ errors are plotted across the bottom.}
\end{figure*}
weaker in the blue side of the troughs between 1989.26 and the later epochs.

The changes in the P\textsubscript{V} line profile occur specifically between the Lick and the FOS observations, which are separated by 1.6 yr in the rest frame of the quasar. The P\textsubscript{V} line did not vary between any of the later observations presented here. However, in Capellupo et al. (2013), we found variability on time-scales as short as 0.25 yr (91 d) in C\textsuperscript{IV} between 2009.22 and 2010.11.

3.2 Line optical depths and total column density

Here, we focus on the Lick 1989.26 observation to derive the column densities of the outflowing gas. We first derive the apparent optical depth versus velocity, $\tau_a(v)$, for the C\textsuperscript{IV}, Si\textsuperscript{IV}, and P\textsubscript{V} BALs.

Using the normalized spectrum, we fit Gaussians to the C\textsuperscript{IV} and Si\textsuperscript{IV} BAL profiles. These Gaussians do not represent any physical properties of the gas; they are simply used to define a smooth fit to the profiles (top two panels of Fig. 3). We then use the equation, $I = I_o e^{-\tau_a}$, to derive $\tau_a(v)$ for the C\textsuperscript{IV} and Si\textsuperscript{IV} lines, where $I_o = 1$ for these normalized spectra. The lines we analyse here, C\textsuperscript{IV}, Si\textsuperscript{IV}, and also P\textsubscript{V}, are all doublets, so deriving $\tau_a(v)$ in this way includes contributions from both transitions at each velocity. We therefore use equation 2 from Junkkarinen, Burbidge & Smith (1983) to remove the doublet structure. The solid and dotted curves in Fig. 4 show the run of apparent optical depths versus velocity, $\tau_a(v)$, for C\textsuperscript{IV} and Si\textsuperscript{IV}, respectively, after removing the doublet structure.

To estimate $\tau_a(v)$ for P\textsubscript{V}, we first take the optical depth profiles for C\textsuperscript{IV} and Si\textsuperscript{IV} and broaden the profiles based on the increased doublet separation in P\textsubscript{V}. We then calculate $I(v)$ from this adjusted $\tau_a(v)$, and fit the resulting C\textsuperscript{IV} and Si\textsuperscript{IV} intensity profiles to the P\textsubscript{V} BAL. The Si\textsuperscript{IV} $I(v)$ profile provided the best fit to the P\textsubscript{V} line, with a small adjustment to the amplitude (bottom panel of Fig. 3; see also, Junkkarinen et al. 1997). We then calculate the P\textsubscript{V} optical
The apparent optical depth profiles for C iv (e.g. fig. 6 in Hamann V 2011 to P abs) are roughly an order 2011 = 1000 for solar abundances. V is the oscillator strength and N IV 444, 3 1998 1000 near the column density lower limits V 1998 τ IV ∼ V V 1998 IV ∼ V V V 1998 IV trough is at least 100 cm IV /m IV BAL, and they conclude that in BALs (see also, Lundgren et al. (2009) and Capellupo et al. (2013) identify other quasars, where a high ratio of Si iv to C iv absorption strength indicates a saturated variable C iv BAL, and they conclude that in these cases, the C iv is likely too saturated to be affected by changes in the ionization of the gas.

Instead, the results presented here (and in Hamann et al. 2008; Capellupo et al. 2013) strongly support the scenario of clouds moving across our line of sight to the quasar continuum source as the cause of the observed variability (see also Leighly et al. 2009; Moe et al. 2009; Hall et al. 2011, Vivek et al. 2012, and references therein). A possible caveat to this interpretation might be that the absorbing region is inhomogeneous, such that it spans a wide range of column densities and line optical depths across our view of the continuum source. In that situation, changes in the continuum flux that change the absorbing region ionization could also change the projected area that has optical depth ≥1 in a given line (i.e. the observed covering fraction), without requiring tangential/crossing motions of the gas (see Hamann et al. 2011, 2012 for more discussion). However, that possibility seems to be contradicted here by our

4 DISCUSSION

4.1 Location of the outflow

In Capellupo et al. (2012) and Capellupo et al. (2013), we discussed the two most likely scenarios for explaining the variability in BALs (see also, Lundgren et al. 2007; Wildy et al. 2014). The first scenario is a change in the quasar’s continuum flux causing global changes in the ionization of the outflowing gas. This could affect the line strengths (optical depths) by changing the column densities in particular ions. There is some evidence for this scenario in outflow lines that vary simultaneously across a wide range in velocities (e.g. Hamann et al. 2011; Capellupo et al. 2012). However, in Q1413+1143 the detection of a P ν BAL indicates that the C iv BAL is very saturated. If the optical depth ratio is τ C IV/P ν > 100 (Section 3.2 above), then the true optical depth across the variable portion of the C iv trough is at least ~70 (cf. Figs 2 and 4). This is much too saturated to be susceptible to changes in the ionization. Similarly, Hamann et al. (2008) and Capellupo et al. (2013) identify other quasars, where a high ratio of Si iv to C iv absorption strength indicates a saturated variable C iv BAL, and they conclude that in these cases, the C iv is likely too saturated to be affected by changes in the ionization of the gas.

Figure 4. The apparent optical depth profiles for C IV, Si IV, and P V, after removing the doublet structure in each line. The C IV and Si IV profiles are derived from the Gaussian fits to the residual intensities in the BALs as shown in Fig. 3, and the P V profile is derived based on the Si IV optical depth profile.

depth profile using this adjusted Si IV I(v) profile and I = I e −τ, and the result is plotted in Fig. 4 as the dash–dotted curve. We note that even though the adjusted Si IV I(v) profile provides the better fit to the P V BAL, it does overestimate the depth of the absorption on the red side of the trough (Fig. 3). This will have a small effect on the column densities we derive, but it does not significantly affect our final results.

We derive apparent ionic column densities for C IV, Si IV, and P V directly from the τ(v) profiles shown in Fig. 4. These column densities, at least for C IV and Si IV, most likely underestimate the true column densities because the lines are probably very saturated (see Section I and the Discussion below). We calculate these values for reference using the following equation:

\[ N = \frac{m_e c}{\pi e^2 f \lambda_0} \int \tau(v) dv, \]

where f is the oscillator strength and \( \lambda_0 \) is the laboratory wavelength (Savage & Sembach 1991). We obtain the following values for the ionic column densities: \( N_{CIV} \sim 1.3 \times 10^{19} \text{ cm}^{-2} \), \( N_{SiIV} \sim 3.6 \times 10^{15} \text{ cm}^{-2} \), and \( N_{PVI} \sim 4.0 \times 10^{15} \text{ cm}^{-2} \).

Given the small number of lines, we measure and the modest constraints they provide on the ionization and column densities, it is sufficient to rely on the published photoionization models by Hamann (1998), Leighly et al. (2009, 2011), and Borguet et al. (2012) to constrain the true optical depths in the C IV BAL and the true total column density, \( N_{HI} \), in the Q1413+1143 outflow. The quasar studied by Borguet et al. (2012) has much narrower absorption lines than Q1413+1143, particularly in P V, and the ionic column densities for C IV, Si IV, and P V are roughly an order of magnitude smaller in the quasar they studied. They also have many more lines detected that provide specific constraints on the outflow physical conditions. Based on those constraints, Borguet et al. (2012) estimate that the true ratio of C IV to P V optical depths should be \( \tau_{CIV}/\tau_{PV} \sim 1200 \) for solar abundances.

Hamann (1998), Leighly et al. (2009), and Leighly et al. (2011) consider a wider range of physical conditions in BAL quasars that more closely resemble Q1413+1143, e.g. with broad P V troughs, similar to C IV, and limited ranges of only higher ions detected. In the BAL quasar studied in Hamann (1998), \( N_{CIV} \) is roughly a factor of 2 smaller than in Q1413+1143, and \( N_{SiIV} \) and \( N_{PVI} \) are roughly a factor of 4 smaller. Hamann (1998) showed that in the limit of low total column densities, where the gas is optically thin throughout the Lyman continuum, the optical depth ratio should be \( \tau_{CIV}/\tau_{PV} \gtrsim 800 \) for solar abundances and any range of ionization conditions. However, those models can be unrealistic if the total columns are too low to yield a detectable P V BAL. Hamann (1998) and Leighly et al. (2009) estimate that the P V detections in the quasars they studied require minimum total column densities of \( N_{HI} \gtrsim 10^{22} \) and \( \gtrsim 10^{22} \text{ cm}^{-2} \), respectively. In that situation, the optical depth ratio should be \( \tau_{CIV}/\tau_{PV} \sim 1000 \) near the column density lower limits and possibly as low as ~100 in extreme circumstances with total columns up to \( 4 \times 10^{23} \text{ cm}^{-2} \) (e.g. fig. 6 in Hamann 1998 and fig. 15 in Leighly et al. 2011). The optical depth ratio in Q1413+1143 should be somewhere in this range.

To estimate the total column density, we first note that the P V BAL in Q1413+1143 is significantly deeper than the quasars measured by Leighly et al. (2009) and especially Hamann (1998), indicating roughly 2–4 times larger P V optical depths and 2–4 times larger P V column densities. If we scale up the column density constraints in Hamann (1998) and Leighly et al. (2009) by a factor of ~2 based on the stronger P V BAL, we estimate that the total outflow column density in Q1413+1143 is conservatively log \( N_{HI} > 22.3 \text{ cm}^{-2} \).
observations of (1) variability in only portions of the BAL troughs (which is a common feature of BALs Capellupo et al. 2012; Filiz Ak et al. 2013), and (2) similar variabilities and observed covering fractions in all three lines of P\textsc{v}, Si\textsc{iv}, and C\textsc{iv} that span a factor of >100 in optical depth.

We therefore adopt the moving cloud model and use the method described in Capellupo et al. (2013) to estimate the location of the gas. This method adopts a simple scenario where a single outflow component of constant ionization and column density crosses our line of sight to the continuum source. The crossing speed we derive from the data depends on the geometry. Capellupo et al. (2013) describe two models for the movement of outflow components across the continuum source (see their fig. 14 for an illustration). First, a circular disc crosses a larger, circular continuum source along a path that continues through the centre of the background continuum source (the ‘crossing disc’ model). In the second model, the absorber, which has a straight edge, moves across a square continuum source (the ‘knife edge’ model). The ‘knife edge’ model is less realistic, especially given the tendency for variability to occur in small portions of BAL troughs (Gibson et al. 2008; Capellupo et al. 2011; Filiz Ak et al. 2013). In the ‘knife edge’ model, the absorber continues to cover a greater percentage of the source over time, until it completely covers the source. This would eventually result in complete absorption at zero intensity. The ‘crossing disc’ model is more realistic, especially in a scenario where separate outflow components, at different velocities, are crossing the background source, causing variability in different portions of the observed spectrum.

We therefore proceed with the ‘crossing disc’ model to calculate the crossing speed of the outflow component. This speed is given by \(D_{1500} \sqrt{\Delta A/\Delta t}\), where \(D_{1500}\) is a characteristic diameter for the continuum source at 1500 Å and \(\Delta A\) is the change in the absorber line-of-sight covering fraction on a time-scale of \(\Delta t\) (Capellupo et al. 2013). For saturated lines like the C\textsc{iv} BAL here, \(\Delta A\) equals the change in absorption strength relative to a normalized continuum. We calculate a \(D_{1500}\) of \(\sim 0.004\) pc using our estimated bolometric luminosity for Q1413+1143 of \(L = 2.4 \times 10^{46}\) erg s\(^{-1}\) (Peterson et al. 2004; Bentz et al. 2007; Gaskell 2008; Hamann & Simon, in preparation).

For \(\Delta A\) and \(\Delta t\), we use results from Capellupo et al. (2013) and the current work. We have more spectra that cover C\textsc{iv} than P\textsc{v}, and the shortest time-scale over which we detect C\textsc{iv} variability is 0.25 yr. The portion of the C\textsc{iv} BAL that varied had a change in absorption depth of \(\Delta A \sim 0.09\) (Capellupo et al. 2013). Since we only observed variability in P\textsc{v} between the Lick 1989.26 and FOS 1994.98 spectra, the maximum variability time-scale for the P\textsc{v} line during the period of our observations is 1.6 yr. The variability in C\textsc{iv} on the shorter time-scale of 0.25 yr occurs over a much smaller portion of the BAL than on the longer time-scale of 1.6 yr. Furthermore, in general, variability over 1.6 yr is much more common than on time-scales of 0.25 yr (Capellupo et al. 2013). Perhaps, the variability seen on the shorter time-scales is caused by smaller components in the flows at small distances, while the bulk of the flow, represented by the larger, more stable BAL feature, resides further out. We adopt the more conservative approach using 1.6 yr as \(\Delta t\) for determining the crossing speed of the outflow, and since the FOS data do not cover the C\textsc{iv} absorption line, we adopt the value of \(\Delta A \sim 0.09\). This gives a crossing speed of 750 km s\(^{-1}\).

Continuing with the procedure of Capellupo et al. (2013), we assume the crossing speed is roughly equal to the Keplerian rotation speed around an SMBH, with a mass of \(M_{\text{BH}} \sim 4.8 \times 10^8 M_\odot\), to get the physical location of the gas. Using the crossing speed based on the ‘crossing discs’ model and the time-scale of 1.6 yr, the distance is \(\sim 3.5\) pc from the central black hole. Since the variability may have occurred over a shorter time-scale, this distance is likely an upper limit.

### 4.2 Energetics of the outflow

The energetics of quasar outflows, and thus their potential to affect the host galaxy and large-scale environments via feedback, is still poorly understood. To estimate the energetics, we first need to know the mass of the flow. If we estimate the flow geometry as part of a thin spherical shell, then the total mass is given by

\[
M \approx 4100 \left(\frac{Q}{15\text{ per cent}}\right) \left(\frac{N_\text{H}}{2 \times 10^{22}\text{ cm}^{-2}}\right) \left(\frac{R}{3.5\text{ pc}}\right)^2 M_\odot,
\]

where \(Q\) is the global covering fraction of the outflow, i.e. the fraction of 4\(\pi\) steradians that the flow covers from the point of view of the central continuum source, \(N_\text{H}\) is the total column density of the flow, and \(R\) is the distance of the flow from the central SMBH (Hamann 2000). We adopt a value of \(Q \sim 15\) per cent based on the fraction of quasars that exhibit BALs in their spectra (Hewett & Foltz 2003; Reichard et al. 2003; Trump et al. 2006; Knigge et al. 2008; Gibson et al. 2009).

For most BAL quasars, it is difficult to constrain \(N_\text{H}\) because few lines are measured and/or the broad profiles blend together and hide the doublet structure in well-studied BALs like C\textsc{iv}. In most cases, the data yield only lower limits on the optical depths and the column densities of the outflowing gas. In this regard, the detection of a low-abundance line such as P\textsc{v} is important because it allows us to estimate the true optical depth in the BALs and better constrain the total column density (see Section 1 and references therein). We adopt the value of \(N_\text{H} \sim 2 \times 10^{22}\) cm\(^{-2}\), based on the apparent optical depth we derive for P\textsc{v} in Q1413+1143 and the photoionization models of Hamann (1998) and Leighly et al. (2009); Section 3.2.

The remaining variable is the radial distance, for which we adopt the value \(R \sim 3.5\) pc derived above from the C\textsc{iv} variations. Note that equation (2) provides only a crude approximation because the value of \(N_\text{H}\) is a lower limit (Section 3.2) while the distance of 3.5 pc is likely an upper limit (Section 4.1). None the less, we can see how changes to these parameters would alter the result. A firm upper limit on the total column in the C\textsc{iv} BAL region is \(N_\text{H} \lesssim 10^{23}\) cm\(^{-2}\) to avoid large electron scattering optical depths that would extinguish all of the near-UV flux. Outflows that are Compton thick are also much too mass loaded to be driven out by radiation pressure (see Hamann et al., in preparation). A lower limit on the radial distance is more difficult to establish, but at \(R\) much smaller than a parsec, it becomes increasingly difficult to maintain the observed moderate degrees of ionization so close to the continuum source (Hamann et al. 2013).

To estimate the mass-loss rates, \(\dot{M}\), we divide the mass in equation (2) by a characteristic flow time, \(t_{\text{flow}} \sim R/v\). We adopt a nominal value of 10 000 km s\(^{-1}\) for the velocity of the flow based on the velocity of the variable interval identified in Figs 1 and 2. At a distance of 3.5 pc, \(t_{\text{flow}} \sim 340\) yr, and the mass-loss rate is therefore \(12 M_\odot\) yr\(^{-1}\). For comparison, we estimate the black hole mass accretion rate with the equation \(L = \eta \dot{M} c^2\), where \(\eta\), the efficiency, is nominally 0.1 (Peterson 1997). For the luminosity, \(L\), we use the bolometric luminosity of \(\sim 2.4 \times 10^{46}\) erg s\(^{-1}\) (Section 2), which gives a mass accretion rate, \(\dot{M}_{\text{acc}}\), of 4.2 \(M_\odot\) yr\(^{-1}\). Hence,
the mass-loss rate through the outflow is roughly three times greater than the mass accretion rate on to the central black hole.

The kinetic energy of the outflow, as defined by \( K = M v^2 / 2 \), is

\[
K \approx 4 \times 10^{44} \left( \frac{M}{4100 M_\odot} \right) \left( \frac{v}{10000 \text{ km s}^{-1}} \right)^2 \text{ erg.} \tag{3}
\]

Dividing by the characteristic flow time, \( t_{\text{flow}} \), gives a time-averaged kinetic luminosity of \( (L_k) \sim 4 \times 10^{44} \text{ erg s}^{-1} \). The ratio of this kinetic energy luminosity to the quasar bolometric luminosity is therefore \( (L_k) / L \sim 0.02 \). This is roughly a factor of three smaller than the ratio of \( (L_e) / L \sim 0.05 \), that is typically cited as the ratio necessary for an outflow to be important for feedback (Scannapieco & Oh 2004; Di Matteo, Springel & Hernquist 2005; Prochaska & Hennawi 2009), but it exceeds the smaller ratio of \( (L_e) / L \sim 0.005 \) estimated theoretically by Hopkins & Elvis (2010). As mentioned above, our estimate of the column density is a lower limit, so if the column density is at least a factor of 2.5 greater, at the maximum distance of 3.5 pc, then the ratio of \( (L_e) / L \) would also exceed the larger threshold of 0.05. Therefore, the outflow might be important for feedback to the host galaxy.

Finally, we point out that the radial distances and kinetic energies derived here, and in other studies of outflow variability (Misawa et al. 2007; Capellupo et al. 2011, 2013; Hall et al. 2011; Hamann et al. 2011, 2013; Rodríguez Hidalgo et al. 2011, 2013; Vivek et al. 2012), are smaller than recent results that use excited-state lines to constrain the outflow densities and radial distances (via photoionization models, e.g. Moe et al. 2009; Dunn et al. 2010; Arav et al. 2013; Borguet et al. 2013). The excited-state absorber studies tend to find distances \( \gtrsim 1 \text{ kpc} \) and kinetic energy luminosities that are important for feedback (sometimes by a large margin). It is not obvious how this apparent discrepancy between the distance results from variability and excited-state lines can be reconciled. It is possible that BAL outflows exist across a wide range of physical scales, perhaps manifesting themselves differently in different quasars. Moe et al. (2009) argue that a variable component of one BAL outflow resides at distances \( \lesssim 0.1 \text{ pc} \) while another component in the same quasar with excited-state lines is at \( R \sim 3.3 \text{ kpc} \). It will be an important test of all of these studies to look for variability in BALs known to have excited-state lines and, conversely, to search for excited-state lines to provide density constraints in BALs systems that vary.

5 CONCLUSIONS

Using the first reported detection of a variable \( \mathrm{P}
\nu \mathrm{BAL} \), we constrain the mass and energetics of the outflow in Q1413+1143. The detection of \( \mathrm{P}
\nu \) absorption, which indicates a very saturated \( \mathrm{C}
\iv \) BAL, and the similar variabilities in the \( \mathrm{P}
\nu \) and \( \mathrm{C}
\iv \) BALs imply that the detected variability is caused by the outflow moving across our line of sight. This crossing clouds scenario provides a constraint on the distance of the outflow from the central SMBH, and the detection of the \( \mathrm{P}
\nu \) BAL, along with photoionization models, constrains the true column density of the flow. Together, these quantities allow us to derive an estimate of the mass and energetics of the flow. Our upper limit for the distance of the flow and the lower limit on the column density gives \( (L_e) / L \sim 0.02 \). This is between the ratio of 0.005 cited by Hopkins & Elvis (2010) and 0.05 determined by earlier work (Scannapieco & Oh 2004; Di Matteo et al. 2005; Prochaska & Hennawi 2009) for an outflow to be sufficiently powerful to affect the host galaxy evolution. Therefore, the outflow in Q1413+1143 might be an important feedback mechanism to its host galaxy.

Using large samples of quasars from the ongoing SDSS-III BOSS survey, which includes many quasars at a large enough redshift to cover the \( \mathrm{P}
\nu \) region, we can search for more detections of \( \mathrm{P}
\nu \) absorption. We can also look for more cases of variable \( \mathrm{P}
\nu \) absorption via repeat observations within SDSS-III and follow-up observations with other telescopes. Estimating column densities and distances for flows in more quasars will better allow us to assess the typical strengths of these outflows and their viability as a feedback mechanism.

ACKNOWLEDGEMENTS

We thank the referee for helpful comments on the manuscript. FH acknowledges support from the USA National Science Foundation grant AST-1009628.

REFERENCES

Adelman-McCarthy J. K. et al., 2008, ApJS, 175, 297
Angonin M.-C., Vanderriest C., Remy M., Surdej J., 1990, A&A, 233, L5
Arav N., Becker R. H., Laurent-Muehleisen S. A., Gregg M. D., White R. L., Brotherton M. S., de Koo M., 1999, ApJ, 524, 566
Arav N., Borguet B., Chamberlain C., Edmonds D., Danforth C., 2013, MNRAS, 436, 3286
Asplund M., Grevesse N., Sauval A. J., Scott P., 2009,ARA&A, 47, 481
Barlow T. A., 1993, PhD thesis, California Univ
Baskin A., Laor A., Hamann F., 2013, MNRAS, 432, 1525
Bentz M. C., Denney K. D., Peterson B. M., Pogge R. W., 2007, in Ho L. C., Wang J.-W., eds, ASP Conf. Ser. Vol. 373, The Central Engine of Active Galactic Nuclei. Astron. Soc. Pac., San Francisco, p. 380
Borguet B. C. J., Edmonds D., Arav N., Benn C., Chamberlain C., 2012, ApJ, 758, 69
Borguet B. C. J., Arav N., Edmonds D., Chamberlain C., Benn C., 2013, ApJ, 762, 49
Capellupo D. M., Hamann F., Shields J. C., Rodríguez Hidalgo P., Barlow T. A., 2011, MNRAS, 413, 908
Capellupo D. M., Hamann F., Shields J. C., Rodríguez Hidalgo P., Barlow T. A., 2012, MNRAS, 422, 3249
Capellupo D. M., Hamann F., Shields J. C., Halpern J. P., Barlow T. A., 2013, MNRAS, 429, 1872
Di Matteo T., Springel V., Hernquist L., 2005, Nature, 434, 604
Dunn J. P. et al., 2010, ApJ, 709, 611
Filiz Ak N. et al., 2013, ApJ, 777, 168
Gabel J. R. et al., 2003, ApJ, 583, 178
Gaskell C. M., 2008, Rev. Mex. Astron. Astrofis. Ser. Conf., 32, 1
Gibson R. R., Brandt W. N., Schneider D. P., Gallagher S. C., 2008, ApJ, 675, 985
Gibson R. R. et al., 2009, ApJ, 692, 758
Hall P. B., Anosov K., White R. L., Brandt W. N., Gregg M. D., Gibson R. R., Becker R. H., Schneider D. P., 2011, MNRAS, 411, 2653
Hamann F., 1998, ApJ, 500, 798
Hamann F., 2000, Quasistellar Objects: Intrinsic AGN Absorption Lines. IoP Publishing, Bristol
Hamann F., Sabra B., Junkarinen V., Cohen R., Shields G., 2002, in Boller T., Komossa S., Kahn S., Kunieda H., Gallo L., eds, Workshop on X-ray Spectroscopy of AGN with Chandra and XMM-Newton, MPE Garching, MPE Report 279, p. 121
Hamann F., Kaplan K. F., Rodríguez Hidalgo P., Prochaska J. X., Herbert-Fort S., 2008, MNRAS, 391, L39
Hamann F., Kanekar N., Prochaska J. X., Murphy M. T., Ellison S. M., Malec A. L., Milutinovic N., Ubachs W., 2011, MNRAS, 410, 1957
Hamann F., Simon L., Hidalgo P. R., Capellupo D., 2012, in Charts G., Hamann F., Leighly K. M., eds, ASP Conf. Ser. Vol. 460, AGN Winds in Charleston. Astron. Soc. Pac., San Francisco, p. 47
Hamann F., Charts G., McGraw S., Rodríguez Hidalgo P., Shields J., Capellupo D., Charlton J., Eracleous M., 2013, MNRAS, 435, 133

MNRAS 444, 1893–1900 (2014)
Hewett P. C., Foltz C. B., 2003, AJ, 125, 1784
Hopkins P. F., Elvis M., 2010, MNRAS, 401, 7
Hutsemékers D., Borguet B., Sluse D., Riaud P., Anguita T., 2010, A&A, 519, A103
Junkkarinen V. T., Burbidge E. M., Smith H. E., 1983, ApJ, 265, 51
Junkkarinen V., Beaver E. A., Burbidge E. M., Cohen R. D., Hamann F., Lyons R. W., 1997, in Aravm N., Shlosman I., Weymann R. J., eds, ASP Conf. Ser. Vol. 128, Mass Ejection from Active Galactic Nuclei. Astron. Soc. Pac., San Francisco, p. 220
Knigge C., Scaringi S., Goad M. R., Cottis C. E., 2008, MNRAS, 386, 1426
Leighty K. M., Hamann F., Casebeer D. A., Grupe D., 2009, ApJ, 701, 176
Leighty K. M., Dietrich M., Barber S., 2011, ApJ, 728, 94
Lundgren B. F., Wilhite B. C., Brunner R. J., Hall P. B., Schneider D. P., York D. G., Vanden Berk D. E., Brinkmann J., 2007, ApJ, 656, 73
Magain P., Surdej J., Swings J.-P., Borgeest U., Kayser R., 1988, Nature, 334, 325
Misawa T., Eracleous M., Charlton J. C., Kashikawa N., 2007, ApJ, 660, 152
Moe M., Arav N., Bautista M. A., Korista K. T., 2009, ApJ, 706, 525
Monier E. M., Turnshek D. A., Lupie O. L., 1998, ApJ, 496, 177
Monier E. M., Turnshek D. A., Rao S., 2009, MNRAS, 397, 943
Peterson B. M., 1997, An Introduction to Active Galactic Nuclei. Cambridge Univ. Press, Cambridge
Peterson B. M. et al., 2004, ApJ, 613, 682
Prochaska J. X., Hennawi J. F., 2009, ApJ, 690, 1558
Reichard T. A. et al., 2003, AJ, 126, 2594
Rodríguez Hidalgo P., Hamann F., Hall P., 2011, MNRAS, 411, 247
Rodríguez Hidalgo P., Eracleous M., Charlton J., Hamann F., Murphy M. T., Nestor D., 2013, ApJ, 775, 14
Savage B. D., Sembach K. R., 1991, ApJ, 379, 245
Scannapieco E., Oh S. P., 2004, ApJ, 608, 62
Trump J. R. et al., 2006, ApJS, 165, 1
Turnshek D. A., 1988, in Blades J. C., Turnshek D. A., Norman C. A., eds, Proc. QSO Absorption Line Meeting: QSO Absorption Lines: Probing the Universe. Cambridge Univ. Press, Cambridge, p. 17
Turnshek D. A., Lupie O. L., Rao S. M., Espey B. R., Sirola C. J., 1997, ApJ, 485, 100
Venturini S., Solomon P. M., 2003, ApJ, 590, 740
Vestergaard M., Peterson B. M., 2005, ApJ, 625, 688
Vivek M., Srianand R., Mahabal A., Kuriakose V. C., 2012, MNRAS, 421, L107
Vivek M., Srianand R., Petitjean P., Noterdaeme P., Mohan V., Mahabal A., Kuriakose V. C., 2012, MNRAS, 423, 2879
Wildy C., Goad M. R., Allen J. T., 2014, MNRAS, 437, 1976

This paper has been typeset from a Ti\TeX\La\TeX file prepared by the author.