Correlations of physiological activities in nocturnal Cheyne–Stokes respiration

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Abstract: We have conducted a power–spectrum–density (PSD) analysis of the distinct sleep stages of a previously diagnosed nocturnal Cheyne–Stokes respiration patient (NCSR) and studied the correlations of different physiological activities. This is the first study where the correlations were analyzed separately for different sleep stages and the influence of arousals was completely eliminated. Mathematical analysis of the polysomnographical records revealed clear indicators of the disorder in the form of large peaks in a very-low frequency range of \( f \approx 0.02 \) Hz. We have shown existence of the significant entrainment of the cerebral and cardiac activities with respiration during different stages of sleep in the patient. The entrainment is highly pronounced in light (stage 2) and deep (stage 3) sleep, but is significantly less pronounced in rapid eye movement sleep. A correlation functions analysis revealed that the correlations between the central activities and respiration attain maximum at negative lag times. Lagging of respiration behind the central activities favors the central hypothesis of generation of NCSR. On the basis of comparison of PSD plots of a NCSR patient and a healthy patient we speculate that the vasomotor center of a NCSR patient assumes the control function in the respiratory control system. Clinical applications of the findings of the study may lead to the development of novel low-cost methods of diagnostic of NCSR based on easy-to-obtain electrocardiogram or electroencephalogram records of patients and emergence of some forms of “substitution therapy”.

Keywords: power–spectrum–density analysis, respiration, sleep stages, periodic breathing

Background
A cyclic breathing pattern characterized by a regular waxing and waning of breathing amplitude and period (T) ranging from 25 to 100 s is a frequently observed sleep disorder.¹⁻⁷ Researchers usually distinguish the cases when the intervals of hyperventilation are separated only by hypopneas (decrease of 50%–90% of the amplitude of airflow lasting 10 s or more) from the cases when both hypopneas and apneas (reduction of >90%) are present between the episodes of hyperventilation. The former patterns are called periodic breathing (PB) while the latter ones are Cheyne–Stokes respiration (CSR). Both patterns may be encountered in sleep and wakeful subjects,⁴⁻¹⁰ in extreme conditions, eg, at high altitudes,¹¹⁻¹³ or normal conditions.¹⁰⁻¹⁴⁻¹⁵ Since its discovery in the mid-19th century, CSR has been associated with congestive heart failure (CHF).⁷ Recently, however, significant evidence has appeared that this type of breathing pattern may come about during sleep in patients without detected CHF.¹⁶⁻¹⁸

The physiological mechanisms responsible for different types of PB are still a matter of debate. Two major hypotheses, however, have received the most attention in the last two decades. The “instability” hypothesis explains PB as a self-sustaining oscillation...
due to the loss of stability in the closed-loop chemical control of ventilation.1–3,14,16,18–22 This loss of stability is thought to be caused by the concurrent presence of slow circulation between lungs and chemoreceptors, enhanced loop gain, and underdumpling of CO2 and O2 that the body stores. Several theoretical models have been suggested to explain PB on the basis of chemical feedback of ventilatory control.2,3,14

The “central” hypothesis, on the contrary, explains PB as the manifestation of a central vasomotor rhythm that modulates ventilation either indirectly through modulation of blood flow23,24 or directly through central irradiation to respiratory centers.25 The instability hypothesis has gained wider acceptance than the central hypothesis mainly because of its sound theoretical basis and use of mathematical models of the respiratory control system.2,17,19 Other hypotheses suggest that PB is just a mechanically and energetically efficient way to deliver oxygen during sleep.11,21

Motivation and objectives

Many clinicians would like to have a simple set of indicators of different cases of PB or CSR in their patient because that can help them determine the treatment strategy. As reported previously,26 oxygen supplementation and continuous positive airway pressure therapy are very helpful for CHF patients but exacerbate the symptoms of obstructive sleep apnea patients by increasing the length and depth of their apneas. It is entirely possible that different types of PB are caused by different physiological mechanisms. However, the case of nocturnal CSR (NCSR) in the patients without detected CHF deserves special attention because more and more patients of sleep centers exhibit this type of sleep disorder.

The main objective of the present research is to study correlations between the central activities (cerebral and cardiac) and respiration that cause PB during sleep in humans. In the present study, only the cases of NCSR in the patients without detected CHF are analyzed. We used the mathematical methods of spectral analysis and correlation functions of time series.27,28 We do not intend to present a comprehensive statistical analysis of a broad cohort of patients; our intention is to analyze a record of a typical NCSR patient. However, it is one of the objectives of the present study to analyze the physiological correlations of the NCSR in different sleep stages.

Methods

Subjects and protocol

The study was not conducted in a clinical setting; it was based on the records of the regular patients of the Sleep and Behavior Medicine Institute (SBMI) in Bannockburn, IL, accredited by the American Academy of Sleep Medicine. Usually patients are referred to SBMI because of a history of sleep disorders. The overnight sleep examinations were performed in the supine position and without use of additional sedatives or hypnotics. Overall, 12 records of the NSCR adult patients aged from 29 to 62 years old have been screened. All NSCR patients and the control subject (no PB symptoms) were free of CHF as assessed by history and physical examination. All records of NSCR patients exhibited similar features. In the present publication we analyze the record of a 58-year-old male patient who later returned to SBMI for treatment. This particular patient was selected from the group of screened NCSR patients because we could ascertain persistence of the symptoms after a significant period of time.

Polysomnography

The clinical evaluations of the patients and all night polysomnograms (PSG) were performed at SBMI using an 18-channel fully computerized system with nasal thermistors to measure the respiration airflow (FLOW) and standard equipment to measure cardiac (electrocardiogram [EKG]) and cerebral (electroencephalogram [EEG]) activities. All measurements were recorded and processed by the commercial software Polysmith 2003 (Neutronics, Inc., Gainesville, FL) using 250 Hz sampling frequency for EEG and EKG channels and 25 Hz sampling frequency for the respiration. Figure 1A is a typical night PSG of a NCSR patient; Figure 1B is the scoring file of the same record as in Figure 1A. The scoring has been done by trained technicians at SBMI using standard criteria,29 which include the differentiation of delta sleep on stages 3 and 4.

Data analysis

The mathematical analysis consisted of two parts: examination of power-spectrum-density (PSD) and correlation-function plots. PSD analysis of PSG recordings was done using custom made software Veeger Fast Fourier Transform (FFT)-Analyzer (EegSoft, Inc., Tempe, AZ). All PSG channels were analyzed in the same range of frequencies from 0.0005 Hz to 0.5 Hz. Correlation functions of the signals could have been obtained from the FFTs of the same signals using the correlation theorem and inverse FFT procedure. However, we found the direct numerical integration method to be more efficient here. The correlation analysis was performed using a program of numerical integration.30 Although the authors conducted only the mathematical analysis of
Physiological activities in nocturnal Cheyne–Stokes respiration

According to the ergodic theorem from the Theory of Stochastic Processes, the same results must come from the analysis of a large group of objects for a short period of time or just one object from the group for a long period of time.\textsuperscript{31} Due to reasons explained above we decided to analyze a record of one typical patient for a full night instead of looking at the random episodes of all the subjects in the cohort. For the statistical fidelity of the results, the analyzed sleep intervals have to be as long as possible and contain as many events of apnea as possible. Large fluctuations in the rate, often associated with body movements, usually occur at the transitions between sleep stages and wake stages. These large fluctuations representing local trends were eliminated because it was our intention to analyze the sleep stages separately and exclude the events of arousals but not the microarousals, which do not disturb the sleep pattern. Arousals are defined as brief – less than 15 s – changes of the EEG pattern without changes of the underlying sleep stage, which may be manifested by incomplete awakenings; microarousals are arousals of duration less than 3 s and not accompanied by any degree of awakening. Thus, from the whole night record there were selected continuous time intervals within the same sleep stage and without arousals. These intervals were called sleep episodes; their durations are shown in the column “Elapsed time” of Table 1. The total

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**Figure 1** Polysomnography of a patient with NCSR.

Notes: The x-axis is time with the scale shown on the bottom of each picture: A) 5 min record from the episode #5 (see Table 1); B) Full night sleepnogram and apnea-hypopnea graph of the same patient.
duration of all the episodes was 5.575 h out of approximately 7 h of the patient’s sleep.

**Results**

**PSD analysis**

Figure 2 shows PSD plots of various channels of the PSG records of a healthy individual with no recognized PB in sleep. PSD of the FLOW channel (Figure 2A) has high density of peaks in the frequency range 0.20–0.25 Hz, which represents normal breathing waves. There is no significant power in the low-frequency range (<0.1 Hz) that characterizes PB. PSD of EKG channel (Figure 2C), in addition to the high-frequency peaks (0.2–0.25 Hz) centered at the normal breathing frequencies, contains two more groups of peaks, mid frequency (0.1–0.2 Hz) and low frequency (0.05 Hz), which are associated respectively with the baroreceptor reflex and vasomotor tone. PSD of EEG channel (Figure 2B) is dominated by the normal breathing waves of high frequencies (0.2–0.3 Hz) and the very slow waves (0.01–0.02 Hz). Both EEG and EKG activities are strongly correlated with respiration in the range of normal breathing frequencies.

PSG of the NCSR patient, Figure 1B, shows that there were apneas in all sleep stages during the night. Recurrent apneas continued from 10 min to several hours and were typically ended by sudden agitated arousals with symptoms of hyperventilation.

Figure 3 represents PSD plots of various activities of the NCSR patient in sleep stage 2. Figure 3A shows that the spectrum of respiration of this patient is dominated by the discrete, narrow peaks within the frequency range of 0.02–0.12 Hz — NCSR frequencies — which are absent from the same plot of a healthy individual (see Figure 2A). The fundamental frequency of instantaneous airflow peaks at 0.025 Hz. This corresponds to $T = 40$ s, which is clearly recognizable on the PSG record (Figure 1A). The amplitude of the fundamental peak is more than an order of magnitude higher than that of the peaks of the normal breathing ($f \sim 0.3$ Hz). The fundamental frequency entails two prominent harmonics at $f' = 0.049$ Hz and $f'' = 0.075$ Hz. Appearance of large harmonics of a fundamental frequency is a clear indication of the nonlinear nature of the respiratory control system.

The powers of EEG and EKG records, Figures 3B and 3C respectively, are also shifted to the lower frequencies compared to that of the healthy patient. The PSD peaks of EEG and EKG channels correlate closely with the PSD peaks of the FLOW channel, Figure 3A, and reach maximum precisely
at the fundamental frequency of NCSR \((f = 0.025 \text{ Hz})\). In addition to the fundamental peak, both cerebral and cardiac activities also have identifiable harmonics of the fundamental one. Interestingly that respiration, Figure 3A, does not have any peaks in the very-low-frequency range \((f < 0.02 \text{ Hz})\), although both central channels (EEG and EKG) have recognizable power in this range.

Figure 4 represents PSD plots of respiration and central activities during sleep-stage 3 of the NCSR patient. Although sleep architecture of the patient does not exhibit many episodes of deep sleep (see Figure 1B), when they occur, their spectral characteristics are very similar to those of light stages (see Figures 3 and 4). The most important features are large amplitudes and narrow peaks of the fundamental NCSR frequency plus a few harmonics and a strong correlation between respiration and central activities.

Contrary to the previous reports that PB is typical for light stages only,\(^1^7\) we are finding that apneas and hypopneas permeate all stages, including rapid eye movement (REM) and deep sleep (see Figure 1B). However, what is true is that the patients who suffer from NCSR syndrome do not go into stage 3 very often and stage 4 not at all. The PSD plot of the FLOW channel during REM sleep stage of the NCSR patient, Figure 5A, shows more equal distribution of power between the NCSR and normal-breathing frequency ranges with a great number of low-frequency waves having significant amplitudes. This means that this stage of sleep is more chaotic (in the sense of dynamical systems), which is reminiscent of a wake stage. PSD of EEG and EKG records (Figures 5B and 5C) also have significant power in the range of NCSR frequencies, but they do not dominate the spectra as in stages 2 and 3. The correlation between respiration
and central activities exists only in the form of increased low-frequency power, but is not as strong as that in sleep stage 2 or 3.

Correlation function analysis
PSD analysis shows clearly that CSR is a state of strong correlations between the central activities and respiration during sleep. The PSD analysis, however, does not shed light on cause–consequence relationship between them. In order to reveal this relationship we analyzed the correlation functions of EEG/FLOW and EKG/FLOW channels of the PSG records of the patients. Specifically we computed the following functions:

\[
\text{corr} < b, f > (\tau) = \frac{1}{t_2 - t_1} \int_{t_1}^{t_2} b(t + \tau) f(t) \, dt
\]

\[
\text{corr} < h, f > (\tau) = \frac{1}{t_2 - t_1} \int_{t_1}^{t_2} h(t + \tau) f(t) \, dt
\]

which are the integrals of the normalized EEG(t), EKG(t), and FLOW(t) channel records superposed and shifted left.
or right in time. The functions in Equation 1 are defined as follows:

\[ b(t) = \frac{EEG(t) - <EEG>}{\sqrt{\text{var}(EEG)}}; \]

\[ h(t) = \frac{EKG(t) - <EKG>}{\sqrt{\text{var}(EKG)}}; \]

\[ f(t) = \frac{FLOW(t) - <FLOW>}{\sqrt{\text{var}(FLOW)}}. \]

where the average and variance of a channel are:

\[ <\text{CHAN}> = \frac{1}{t_2 - t_1} \int_{t_1}^{t_2} \text{CHAN}(t) dt; \]

\[ \text{var}(\text{CHAN}) = \frac{1}{t_2 - t_1} \int_{t_1}^{t_2} [\text{CHAN}(t) - <\text{CHAN}>]^2 dt; \]

\[ \text{CHAN}(t) = EEG(t); EKG(t); FLOW(t). \]

Because the actual records are represented in the form of time series instead of a continuous function, all integrals
in Equations 1–3 were replaced by their discrete equivalents according to:

\[
\frac{1}{t_2-t_1} \sum_{i=1}^{N} \left\{ \cdots \right\} dt \rightarrow \frac{1}{N} \sum_{i=1}^{N} \left\{ \cdots \right\}
\]

(4)

The correlation function is large at some positive (negative) value of the time lag \( \tau \) if the first function is a close copy of the second one but is shifted to the right (left) of the second.

Figure 6 is a plot of the EEG/FLOW and EKG/FLOW correlation functions of the healthy patient. They have an obvious high frequency periodicity \( (T = 4 \text{ s}) \) due to normal respiration, which is easily observed on PSD plots in the form of the peaks in the normal-breathing range \( (0.2–0.25 \text{ Hz}) \); see Figure 2). The high frequency modulation of the correlation functions is not of interest in the present study and could have been removed through some kind of coarse-graining procedure, eg, detrending.\(^{27}\) It did not present a significant obstacle in the present analysis and, hence, was not removed. The EKG/FLOW correlation function has a low-frequency modulation \( (T = 30 \text{ s}) \), which is due to low-frequency waves of cardiac activity driven by the vasomotor tone, Figure 2C. The EEG/FLOW correlation...
function also has the low-frequency modulation, but less pronounced (has smaller amplitude).

The plots of the EEG/FLOW and EKG/FLOW correlation functions of the NCSR patient in sleep stages 2 and 3 are depicted in Figures 7 and 8, (A) and (B), respectively. The low-frequency modulation (NCSR frequencies, $T \approx 40$ s) is more pronounced (has greater amplitude) than the high-frequency one (normal-breathing frequencies, $T \approx 3$ s). This fact is also prominent on the PSD plots of the respective episodes, Figures 3 and 4, in the form of large amplitudes of the NCSR waves. Interestingly, the amplitude of $corr_{<b,f>} (\tau)$ is more than twice the amplitude of $corr_{<h,f>} (\tau)$, while for the healthy subject they are practically equal. It would have been interesting to extend the correlation analysis beyond $T = 100$ s, but this was not possible due to limited duration of episodes. Figure 9 presents correlation functions in REM sleep stage. While the high-frequency modulations are practically of the same scale as in stages 2 or 3, the low frequency amplitudes are significantly smaller than in stages 2 or 3. This fact may also be confirmed on PSD plots of the corresponding channels (Figures 3–5).
To characterize the cause–consequence relationship between the time series we introduce respectively the time lags of maximum correlation of the cerebral and cardiac activities with the respiration:

\[
\hat{\tau}_{b,f} = \tau \{ \text{corr}<b,f>(\tau) \Rightarrow \text{max} \}
\]

\[
\hat{\tau}_{h,f} = \tau \{ \text{corr}<h,f>(\tau) \Rightarrow \text{max} \}
\]  

(5)

The maximum-correlation time lags for EEG/FLOW and EKG/FLOW correlation functions of the healthy patient were practically zero. Table 1 contains the lag times of maximum correlation of the EEG/FLOW and EKG/FLOW activities for the NCSR patient. More than 75% of the lag times are negative (\(\hat{\tau}_{b,f} < 0, \hat{\tau}_{h,f} < 0\)), with the average values of \(<\hat{\tau}_{b,f}> = -1.57s, <\hat{\tau}_{h,f}> = -1.25s\). Moreover, there are no episodes where the cerebral and cardiac time lags are both positive. The analysis of the data proves statistical significance of the revealed correlation. Together with the fact that for the healthy patient the maximum-correlation time

Figure 8 Correlation functions of sleep stage 3 episode #9 (see Table 1) of an NCSR patient: A) EEG/FLOW; B) EKG/FLOW.

Abbreviations: EEG, electroencephalogram; EKG, electrocardiogram; FLOW, respiration airflow; NCSR, nocturnal Cheyne-Stokes respiration.

Figure 9 Correlation functions of REM sleep-stage episode #3 (see Table 1) of an NCSR patient: A) EEG/FLOW; B) EKG/FLOW.

Abbreviations: EEG, electroencephalogram; EKG, electrocardiogram; FLOW, respiration airflow; NCSR, nocturnal Cheyne–Stokes respiration; REM, rapid eye movement.
lags were practically zero, this leads us to the conclusion that NCSR is generated by variations in central nervous activity. In other words, the results of the present study favor the central hypothesis of the origin of NCSR.

Discussion

We have conducted the PSD analysis of the distinct sleep stages of previously diagnosed NCSR patients and studied correlations of the different physiological activities in them. In this publication we present analysis of the full-night record of a typical NCSR patient. The statistical analysis of the data proved the significance of our findings. This is the first study where the correlations were analyzed separately for different sleep stages and the influence of the arousals was completely eliminated. Mathematical analysis of PSG records of the NCSR patient revealed clear indicators of this type of disorder in the form of a large peak in a very-low-frequency range of $f = 0.02$ Hz. We have shown existence of the significant entrainment of the cerebral and cardiac activities with respiration during different stages of sleep in the NCSR patient. The entrainment is highly pronounced in light (stage 2) and deep (stage 3) sleep, and is significantly less pronounced in REM sleep. This result may lead to the development of novel low-cost methods of diagnosis of NCSR based on easy-to-obtain EKG records of patients.

The simple PSD analysis, however, did not shed light on causal nature of the nocturnal PB. A correlation functions analysis revealed that the correlations between the central activities and respiration attain maximum at negative lag times. Lagging of respiration behind the central activities in NCSR patients cannot be explained simply by the time for propagation of the neuronal impulses from the brain-stem to the plant because, first, the healthy patient did not have this type of lagging, and, second, neither EEG nor EKG are likely to detect this type of activity.

Comparing PSD plots of a NCSR and healthy patients, one can notice that the NCSR frequencies are close to the frequencies of the vasomotor tone. Thus, the results of the present study suggest that, at least for the analyzed patient, “the prime generator of CSR is variations in the central nervous regulatory activity, which, in turn, is influenced by factors such as heart failure”.25 According to this hypothesis, the vasomotor center of a NCSR patient assumes the control function in the respiratory control system. Franklin et al also speculated that “CSR is a physiological life-saving mechanism when a vital organ such as the heart or the brain has been severely damaged”.25 In this case CSR is an example of compensatory mechanism of physiological disorders, which has been considered recently by the present authors in the general framework of control system theory.55 To prove or disprove this hypothesis we are planning an experimental application of periodic vibrostimulation during sleep of a patient with NCSR. If the hypothesis is correct, the patient will respond to such stimulation by complete elimination of apneas or at least in significant decrease of its frequency. In this case the findings of the present study can have clinical applications. For instance, one may foresee development of some forms of low-cost EKG- or EEG-based “substitution therapy” for CSR.

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Disclosure

The authors report no conflicts of interest in this work.

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