Effects of low work-function lanthanum oxides on stable electron field emissions from nanoscale emitters

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Nanoscale electron field emitters are known to produce more stable electron emissions than conventional emitters. This has been attributed to size effects; nanoscale emitters can operate with a small emission current and a low extraction voltage, which reduces the bombardment of residual gas ions on the emitter tip. However, our experiments discovered that nanoscale LaB₆ emitters had extremely stable emissions, suggesting that chemical effects are present in addition to size effects. This suggests that during operations, a material other than LaB₆ may be deposited on the surface of the tip to enhance the stability of emissions. Therefore, we searched for possible materials theoretically within the La–B–O ternary system and found that lanthanum oxides (LaO) and oxygen-deficient La₂O₃ (La₂O₃₋ₓ) had good electrical conductivity and a low work function comparable to that of LaB₆. These lanthanum oxides are chemically less reactive to residual gases than LaB₆. Thus, if they are present on the LaB₆ surface, they could stabilize electron emissions without diminishing the emission performance. These findings suggest that lanthanum oxides could be used for electron field emitters.

1. Introduction

Electron guns have been used for decades in various instruments, including cathode-ray tubes, electron microscopes, and electron-beam lithography systems. They can be classified into the following types of electron emissions: thermionic emissions (TE), Schottky emissions (SE), thermal field emissions (TFE), and cold field emissions (CFE). Electron source materials are chosen to correspond to each emission type, for instance, tungsten (W) for TE and CFE, LaB₆ and CeB₆ for TE, and tungsten coated with zirconium oxide (W/ZrO) for SE.1–11

Currently, W is used for the emitter tip of CFE electron guns because it can be processed to dimensions less than 100 nm, which is necessary to create a high electric field (>10⁸ V m⁻¹) and produce a fairly constant emission current. Many studies have been conducted to find electron source materials with superior emission properties, for example, single-atom tips,12–16 carbon nanotubes,17–19 and etched sharp tips of borides,20–26 carbides,27–30 and nitrides.31–39

In particular, LaB₆ has been studied repeatedly since the 1970s because its low work function (WF) (2.1–2.6 eV) and chemical stability made it ideal as a TE emitter. Earlier studies of CFE from a LaB₆ tip found that the emission current was not sufficiently stable and decayed after several minutes.40 Since around the year 2000, advanced technologies have been implemented to fabricate nanoscale LaB₆ emitters.15–24 A LaB₆ nanowire with a thickness of less than 100 nm has been synthesized by chemical vapor deposition (CVD).21 When applied to an electron emitter, the LaB₆ nanowire produced a stable CFE.22–24 Notably, the emission current exhibited extreme stability without decay for over tens of hours.24 Furthermore, a LaB₆ nanoneedle created by focused ion beam (FIB) milling demonstrated a higher degree of stability than nanowires and greatly exceeded the performance of the W emitter.23 The LaB₆ nanoneedle emitter was assembled in a TEM and was capable of long-term stable (<1%/100 h) atomic imaging, which has never been achieved by other CFE electron sources.26

The reason for the high current stability is attributed to the following:1 (i) to achieve the same probe current, the total emission current for the nanoscale emitter is several orders of magnitude smaller than that of the conventional emitter, which reduces the generation of residual gas ions and consequently reduces the ion bombardment on the emitter tip; (ii) the lower extraction voltage for the nanoscale emitter is also advantageous for reducing residual gas ions and damage caused by the ion bombardment. In addition, we proposed another possible factor in our previous study;25 (iii) the electric current density in...
the apex region becomes so intense ($\sim 10^6$ A cm$^{-2}$) that electrons provide kinetic momentum to the adatoms on the surface, inducing an atomic flow toward the apex (electromigration) and eventually enhancing the desorption rate of the adatoms.

The above findings are size effects that apply to all nanoscale emitters. In addition to size effects, it appeared in our experiments$^{24,25}$ that chemical effects might also have been observed on the nanoscale LaB$_6$ emitters, that is, a material other than LaB$_6$ was deposited on the surface, and it enhanced the current stability. We conceived this idea after noticing that the energy-dispersive X-ray spectroscopy (EDS) image of the nanoneedle tip appeared to show a reduction of boron atoms on the surface layers.$^{25}$

Although the EDS analysis suggested the presence of chemical effects, it was not decisive enough to reach this conclusion. Therefore, in this study, we theoretically investigated whether chemical effects occur on the nanoscale LaB$_6$ tip and attempted to identify the materials covering the surface. The study was conducted for the most part using first-principles calculations and molecular dynamics (MD) simulations. We extensively searched for materials in the phase diagram that satisfied the required conditions for stabilizing the emission current.

2. Calculation methods

The calculations of the electronic structures and Car–Parrinello MD simulations were conducted using the Quantum ESPRESSO code,$^{47,48}$ based on density functional theory with plane waves and pseudopotentials. The ultrasoft pseudopotentials$^{49}$ were adopted from the library of Quantum ESPRESSO.$^{49}$ The generalized gradient approximation functional of Perdew, Burke, and Ernzerhof was employed.$^{50}$ An energy cut-off of 80 Ry for plane waves and 560 Ry for electron density were sufficient to provide the convergence of the total energy. The DOS and WF were calculated following the optimization of the lattice parameters and the atomic structures using Monkhorst-Pack $k$-point sampling$^{51}$ with an $8 \times 8 \times 8$ mesh for the unit cell. The calculated lattice parameters were within an error of 1% from the corresponding experimental values.

Slab models were used for the WF calculations and MD simulations, which comprised several atomic layers separated by a vacuum layer of 15 Å. The WF $\phi$ was estimated using the following formula$^{51}$

$$\phi = V_{\text{vac}} - E_f$$  

(1)

where $V_{\text{vac}}$ and $E_f$ are the electrostatic potential of vacuum and the Fermi energy, respectively. In the MD simulations, the time step was taken as about 0.06 fs, and the temperature was controlled by rescaling the total kinetic energy of the atoms. All calculations were carried out using the Numerical Materials Simulator supercomputer at NIMS.

3. Results and discussion

According to the EDS analysis,$^{25}$ the atomic elements detected on the outermost surface of the LaB$_6$ emitter were La, B, and O. Therefore, we searched for materials consisting of these three elements. Since hydrogen is not detected by EDS, the possibility of the synthesis of hydroxides cannot be excluded. This is discussed in Section 3.5. As there appear to be no experimental phase diagrams available for the ternary La–B–O system, we calculated the theoretical phase diagram using the Open Quantum Materials Database (OQMD).$^{54}$ The calculation method for judging the stability of compounds was based on DFT + U$^{55}$ and the Quickhull algorithm.$^{56}$

The results are shown in Fig. 1, where stable and unstable (metastable) compounds are represented by green and red circles, respectively. There are some other unstable compounds omitted from the figure. La$_3$BO$_6$, denoted by the yellow circle, did not appear in this calculation although its existence has been experimentally confirmed.$^{57-59}$ Therefore, it is added to Fig. 1. As the stable compounds are aligned along the lines of B–La, La–O, B–O, and B$_2$O$_3$–La$_2$O$_3$ binary systems, we searched for possible materials covering the LaB$_6$ tip along these binary lines.

3.1. Lanthanum borides

First, we considered LaB$_4$ in the B–La system as a potential covering material because of the following: (i) it is metallic$^{60}$ (ii) it has been observed on oxidized LaB$_6$ surfaces;$^{61-63}$ (iii) it is structurally similar to LaB$_6$. The covering materials must be conductive; otherwise, they will obstruct electron emissions from the surfaces. LaB$_4$ has a tetragonal crystal structure, including octahedral B$_6$ clusters, like LaB$_6$. By analogy with LaB$_6$, we expected that LaB$_4$ would have a lower WF when its surface was terminated by a La layer, and we calculated the WF of the La-terminated LaB$_4$ (001) surface using a slab model of (1 $\times$ 1 $\times$ 6) unit cells separated by a 15 Å space. The result showed that the WF of the La-terminated surface was about 3.2 eV, and that of the opposite surface, terminated by a B layer, was about 4.5 eV. In contrast to our expectations, the WF of LaB$_4$ was much higher than that of LaB$_6$, meaning that LaB$_4$ would diminish the performance of the LaB$_6$ emitter if present on the surface. Consequently, LaB$_4$ could not be a candidate material.

Fig. 1 Calculated ternary phase diagram of the La–B–O system. Green and red circles denote stable and unstable (metastable) compounds, respectively. See the text for the yellow circle (La$_3$BO$_6$).
3.2. Lanthanum monoxide LaO

Except for LaB₄, no stable materials in the phase diagram (Fig. 1) are as conductive as LaB₆. However, LaO (NaCl structure), though judged to be unstable, has been reported to be metallic.⁶⁶–⁶⁸ It was synthesized for the first time under high pressure⁶⁶ and recently as a thin film on substrates.⁶⁷,⁶⁸ Thin films of high-pressure phases sometimes appear because of the stress applied by the interface. Notably, LaO was also observed in the LaB₆ oxidation experiment.⁶⁹ For these reasons, we anticipated that LaO could be a covering material, and we calculated the electronic density of states (DOS) and the WF.

The DOS of LaO shown in Fig. 2 indicates that it is metallic, which is consistent with previous experimental and theoretical results.⁶⁶–⁶⁸ The states at the Fermi level originate mostly from the d-orbitals of the La atoms. The WF of the LaO(001) surface was calculated employing the slab model shown in the inset of Fig. 2. The model consisted of six layers of LaO separated by a 15 Å space fully optimized before the WF calculation. The calculated WF was approximately 2.3 eV, which is very close to that of LaB₆. Therefore, LaO does not greatly diminish electron emissions even if it covers the LaB₆ surface. It was not previously known that LaO has a WF as low as that of LaB₆. LaO could be applied to electron emitters if it generates stable electron emissions.

If LaO is chemically stable and can cover the LaB₆ emitter, it would stabilize electron emissions. To investigate the chemical stability of LaO, we conducted Car–Parrinello MD simulations of gas molecule adsorption under the operating conditions of the emitter. For the (001) surfaces of LaB₆ and LaO, slab models of (2 × 2 × 3) unit cells were employed (Fig. 3), on which the gas molecules H₂, O₂, H₂O, and CO were initially placed at a height of 4 Å from the surface. Although the operating temperature of the emitter tip is uncertain, it should be slightly higher than room temperature and was assumed to be 500 K in the simulations. The actual temperature would not exceed this because the energy dispersion of the emitted electron beam was small.²⁵ The duration of the simulations was 1.5 to 3.0 ps.

In the case of H₂O adsorption, the H₂O molecule spontaneously dissolved and was chemisorbed on LaB₆(001) (Fig. 3, top left) with the H atom on a B atom and the OH on a La atom. In contrast, the H₂O molecule did not immediately dissolve on LaO(001) (top right). With regard to O₂ adsorption, the O₂ molecule was dissolved and chemisorbed on LaB₆(001) (Fig. 3, bottom left) with O atoms on B atoms when the WF was increased by 0.13 eV. Similarly, the O₂ molecule was dissolved on LaO(001), but the O atoms seemed to be absorbed into the bulk (bottom right). This suggests that LaO spontaneously transforms into the more stable La₂O₃ phase when plenty of O atoms are supplied. Since the adsorbed O atoms are far fewer than the bulk O atoms, LaO does not transform into La₂O₃ in the present case. The WF of LaO(001) hardly increased upon O₂ adsorption, probably because the dissolved O atoms did not remain on the surface, and the DOS of the bulk underwent little change with the additional O atoms. As for H₂ and CO adsorptions, the H₂ molecule was not adsorbed on LaB₆(001) or LaO(001), and the CO molecule was adsorbed but not dissolved on these surfaces. The observed inactivity of H₂ on the LaB₆ surfaces was consistent with experimental results.⁷⁰

Although the duration time and the initial conditions were limited, the results of the MD simulations suggest that the LaO(001) surface was chemically as stable as, or slightly more stable than, the LaB₆(001) surface. The LaO(001) surface was not resistant to oxidation; however, it would appear to be resistant in practice because the WF was hardly influenced by oxidation. Consequently, LaO is a candidate for the materials covering the LaB₆ tip.
3.3. Lanthanum oxides \( \text{La}_2\text{O}_3 \) and \( \text{LaO}_2 \)

Along with \( \text{LaO} \), a large amount of \( \text{La}_2\text{O}_3 \) was observed in the \( \text{LaB}_6 \) oxidation experiment. This is to be expected because \( \text{La}_2\text{O}_3 \) is the most stable phase in the \( \text{La}-\text{O} \) binary system (Fig. 1). \( \text{La}_2\text{O}_3 \) is a potential high- \( \text{H}_2\text{O} \)-vacancies \( (\text{La}_2\text{O}_3) \) material that can be used for semiconductor devices. \( \text{LaB}_6 \) is the most stable phase in the \( \text{La} \) \( \text{O}_2 \) binary system. When it is applied to gate insulators, the leak current becomes a problem in the presence of oxygen vacancies, even at low temperatures. The vacancies are supposed to work as donors and induce the electric current of Poole–Frenkel types and space-charge limited types.

Having adequate electrical conductivity, \( \text{La}_2\text{O}_3 \) with \( \text{O} \) vacancies \( (\text{La}_2\text{O}_{3-x}) \) would not obstruct emissions from the \( \text{LaB}_6 \) tip and would serve as \( \text{LaO} \) if the WF is sufficiently low. The DOS and WF calculations for \( \text{La}_2\text{O}_{3-x} \) require attention because of its polymorphism. \( \text{La}_2\text{O}_3 \) of hexagonal \( (\text{space group } \text{P}3\text{m}1) \), monoclinic \( (\text{C}2/\text{m}) \), and cubic \( (\text{Ia}3) \) structures have been observed in the \( \text{LaB}_6 \) oxidation experiment. With the inclusion of another reported cubic phase \( (\text{LaO}_{1.5}, \text{Im}3\text{m}) \), we investigated the electronic structures of \( \text{La}_2\text{O}_{3-x} \) in these four crystal structures.

In the cubic \( (\text{Im}3\text{m}) \) phase, the oxygen sites are split and randomized, as such a structure cannot be realized using a single unit cell. An approximate structure model was constructed employing a \((2 \times 2 \times 2)\) cell with the oxygen positions randomized by MD simulations and annealing. There is an additional hexagonal phase \( (\text{P}6_3/\text{mmc}) \), but it is merely a variant of the hexagonal \( (\text{P}3\text{m}1) \) phase with split oxygen sites and, therefore, was excluded from the calculations. There are several oxygen sites in hexagonal and monoclinic structures. To create vacancies, an \( \text{O} \) atom was removed from each structure to attain the lowest total energy. For the hexagonal phase, an \( \text{O} \) atom coordinated with six \( \text{La} \) atoms was removed, and for the monoclinic phase, an \( \text{O} \) atom coordinated with five \( \text{La} \) atoms was removed.

Fig. 4 shows the DOS of hexagonal \( \text{La}_2\text{O}_3 \) \((\text{no vacancies})\) and four polymorphs of \( \text{La}_2\text{O}_{3-x} \) \((\text{with vacancies})\) mentioned above. The concentrations of \( \text{O} \) vacancies were adjusted to about 5% in the calculations, depending on the number of atoms in the unit cell. In all the structures, it was observed that \( \text{O} \) vacancies generated new states near the bottom of the conduction band, and the Fermi level laid at the top of the new states. The band gaps from the new states to the conduction band were less than 0.5 eV, so the materials practically became conductive by the thermal excitation of the electrons. The values of the band gap correspond to the energy difference between the vacuum level and the bottom of the conduction band. The good agreement between the calculated and experimental values affirms the validity of the choice of the neutral surfaces. \( \text{La}_2\text{O}_{3-x} \), with such a low WF, would not diminish the emission performance of the \( \text{LaB}_6 \) tip.

![Image](https://example.com/image.png)

**Fig. 4** Electronic DOS of \( \text{La}_2\text{O}_3 \) and \( \text{La}_2\text{O}_{3-x} \). (a) no defects, (b) hexagonal with \( x = 0.125 \), (c) monoclinic with \( x = 0.167 \), (d) cubic \( (\text{Ia}3) \) with \( x = 0.125 \), and (e) cubic \( (\text{Im}3\text{m}) \) with \( x = 0.125 \). The insets depict the surfaces on which the WF was calculated.

### Table 1: Calculated work functions (WFs) of La oxides, hydroxide, and borides

| Material           | WF (eV) | Surface |
|--------------------|---------|---------|
| \( \text{LaO} \)   | 2.3     | (001)   |
| \( \text{La}_2\text{O}_{3-x} \), hexagonal | 1.8 | (1120) |
| \( \text{La}_2\text{O}_{3-x} \), monoclinic | 2.0 | (010) |
| \( \text{La}_2\text{O}_{3-x} \), cubic \( (\text{Ia}3) \) | 1.9 | (110) |
| \( \text{La}_2\text{O}_{3-x} \), cubic \( (\text{Im}3\text{m}) \) | 2.1 | (001) |
| \( \text{La(OH)}_{1-x} \) | 1.9 | (0001) |
| \( \text{LaB}_6 \) | 2.3 | (001) |
| \( \text{LaB}_4 \) | 3.2 | (001) |

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To investigate the chemical stability of La$_2$O$_{3-x}$, as was done for LaO (Fig. 3), MD simulations were conducted with H$_2$O, O$_2$, H$_2$, and CO molecules on the (110) surface of hexagonal La$_2$O$_{3-x}$ (Fig. 4b inset). The conditions of the MD simulations were the same as for LaO (500 K and 3 ps). As a result, these molecules did not dissolve on the surface within the simulation time. Since the electronic states of other polymorphs of La$_2$O$_{3-x}$ are very similar to the hexagonal one, the results indicate that the La$_2$O$_{3-x}$ surfaces are more stable than the LaB$_6$(001) and LaO(001) surfaces. Taking the low WF and high chemical stability into consideration, La$_2$O$_{3-x}$ can be a covering material for the LaB$_6$ tip and may function as an electron emitter.

According to the calculated phase diagram (Fig. 1), LaO$_2$ was classified as being in a stable phase. However, there have been no experimental reports on the synthesis of LaO$_2$; there is only a theoretical prediction of it. We investigated the electronic structure of LaO$_2$, based on the atomic structure provided by Marques et al. When the structure was optimized, it appeared to be locally stable. The calculated DOS showed that LaO$_2$ was an insulator with a band gap of approximately 3 eV. When an O vacancy was introduced, it remained an insulator without any change in the value of the band gap. This is probably because O atoms are redundant in LaO$_2$ to complete the ionic bonds with the La atoms. Since both La$_2$O$_3$ and LaO$_2$ are insulators, all compounds between them (LaO$_{3-x}$, $1.5 \leq x \leq 2.0$) are very likely to be insulators and would obstruct emissions from the LaB$_6$ tip.

### 3.4. Lanthanum borates, metaborates, and boron oxides

By analogy with La$_2$O$_3$, we considered that borates, metaborates, and boron oxides in the phase diagram (Fig. 1) might possibly have the same properties as La$_2$O$_3$, and we calculated the electronic structures of LaBO$_3$, LaB$_2$O$_6$, B$_2$O$_3$, and B$_2$O in the presence of O vacancies. LaBO$_3$, denoted by the yellow circle in Fig. 1, was excluded from the considerations because its crystal structure is unknown. Its properties will be inferred from the results for LaBO$_3$ and LaB$_2$O$_6$. Regarding LaB$_2$O$_6$, it has two O sites, one coordinated with a La atom and the other with two La atoms. An O atom was removed from the former site to reduce the total energy.

Fig. 5 shows the calculated DOS of these materials with O vacancies. For LaBO$_{3-x}$ (a), LaB$_2$O$_{6-x}$ (b), and B$_2$O$_{3-x}$ (c), the defect levels (blue arrows) appear in the middle of the original band gap. For B$_2$O$_{3-x}$ (d), an unoccupied defect level is located at the bottom of the conduction band. In the DOS of B$_2$O$_{3-x}$ (c), LaB$_2$O$_{6-x}$ (b), and LaBO$_{3-x}$ (a), the defect levels shift upward as the composition approaches LaBO$_3$ on the B$_2$O$_3$–LaO$_2$ line (Fig. 1). This is consistent with the results for La$_2$O$_{3-x}$, where the defect levels were at the bottom of the conduction band (Fig. 4). Since LaB$_2$O$_6$ is located at the midpoint between LaBO$_3$ and LaO$_2$ in the phase diagram (Fig. 1), it is reasonable to infer that LaB$_2$O$_6$ with O vacancies still had a band gap. Thus, the La borates, metaborates, and boron oxides cannot be conductive even in the presence of O vacancies and are unlikely to cover the LaB$_6$ tip.

### 3.5. Lanthanum hydroxide La(OH)$_3$

Except for the ternary compounds presented in Fig. 1, it is known that La(OH)$_3$ is produced from La$_2$O$_3$ by a simple hydration reaction. We therefore investigated the possibility that La(OH)$_3$ might become conductive when defects are introduced. The DOS of La(OH)$_3$ was calculated with OH vacancies instead of O vacancies because O and H atoms are paired in the structure. The DOS of La(OH)$_{3-x}$ (Fig. 6) is similar to that of La$_2$O$_{3-x}$ (Fig. 4), where the defect levels appear at the bottom of the conduction band, which makes La(OH)$_{3-x}$ as conductive as La$_2$O$_{3-x}$. The WF of La(OH)$_{3-x}$ calculated on the neutral [0001] surface (Fig. 6 inset) was approximately 1.9 eV, which is comparable to that of La$_2$O$_{3-x}$ and LaO (Table 1). Thus, La(OH)$_{3-x}$ could be a covering material for the LaB$_6$ tip. However, La(OH)$_3$ dehydrates at 330 °C and converts to La$_2$O$_3$, so in this case, La(OH)$_3$ does not need to be considered because the emitter tip was cleaned by flash heating at about 800 °C.

### 3.6. Synthesis mechanism of LaO and La$_2$O$_3$

Our theoretical studies found that LaO and La$_2$O$_{3-x}$ could enhance the chemical stability of the LaB$_6$ emitter without...
degrading the emission performance. If these La oxides were present on the LaB₆ surface, we can surmise their synthesis mechanism from the various experiments we describe below.

When a LaB₆ crystal is exposed to an oxygen atmosphere, O₂ molecules are dissociatively adsorbed on the surface even at room temperature.⁸⁰⁻⁸⁵ When the crystal is heated in an oxygen atmosphere to around 500–700 °C, the surface starts to be oxidized to yield LaOₓ, LaₓO₃₋ₓ, B₂O₃, LaBO₃, LaB₂O₆, and La₃BO₆ on the macroscopic scale.⁸⁶⁻⁸⁸ However, in our experimental conditions, the LaB₆ tip was heated for cleaning in an ultrahigh vacuum, where the desorption processes are as significant as the oxidation processes. The oxide layers would then be limited to several atomic layers. In the thermal desorption experiments,⁸¹⁻⁸² B oxides in the forms of BO and B₂O₂ began to desorb at temperatures around 1000 K (727 °C), and La oxides in the form of LaO desorbed at higher temperatures of around 1400 K (1127 °C). At about 1500 °C, the LaB₆ surface became clean.¹¹ In our experiments,²⁵ the LaB₆ tip was heated at a moderate temperature of around 800 °C, which would incidentally have B oxides desorb and La oxides remain on the surface.

Regarding La borates and metabolates (LaBO₃, LaB₂O₆, and La₃BO₆) that have been synthesized in an oxygen atmosphere,⁶⁹⁻⁸⁶ it is uncertain whether they can be synthesized under oxygen-depleted conditions. Considering the fact that these materials are synthesized at temperatures (∼900 °C) slightly higher than the temperature at which boron oxides BO and B₂O₂ are desorbed in a vacuum (727 °C),⁸¹⁻⁸² it seems unlikely that La borates and metabolates are preferably synthesized on the LaB₆ surface in an ultrahigh vacuum.

4. Conclusions

In order to examine possible chemical effects on LaB₆ nanoscale emitters, we searched for materials that could cover the emitter tip to stabilize electron emissions during long operating times. Extensive studies, based on the ternary phase diagram of the La–B–O system, showed that LaO and LaₓO₃₋ₓ could serve as the covering material. Compared with LaB₆, these materials have higher chemical stability against typical residual gases (H₂, O₂, H₂O, and CO) and have an equivalently low WF, which enables the emitter to maintain excellent emission performance. It should be noted that these chemical effects can coexist with size effects. It is presumed that flash heating at a moderate temperature of around 800 °C played a crucial role in the LaB₆ tip having LaO and/or LaₓO₃₋ₓ layers, where B oxides are selectively desorbed and La oxides remain on the surface. It was recognized for the first time that LaO and LaₓO₃₋ₓ have such a low WF that they could be used for electron emitters.

Author contributions

W. H. conducted theoretical calculations and wrote the initial draft. S. T. performed the experiments and provided extensive comments on the manuscript. J. T. and L.-C. Q. managed the entire research project. All authors contributed to the discussion.

Conflicts of interest

There are no conflicts to declare.

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References

1. L. W. Swanson and G. A. Schwind, Adv. Imaging Electron Phys., 2009, 159, 63–100.
2. L. W. Swanson and G. A. Schwind, in Handbook of Charged Particle Optics, ed. J. Orloff, CRC Press, New York, 2nd edn, 2008, ch. 1, pp. 1–28.
3. R. G. Forbes, in Handbook of Charged Particle Optics, ed. J. Orloff, CRC Press, New York, 2nd edn, 2008, ch. 3, pp. 87–128.
4. N. D. Lang, A. Yacoby and Y. Imry, Phys. Rev. Lett., 1989, 63, 1499–1502.
5. H. Kuo, I. Hwang, T. Fu, J. Wu, C. Chang and T. Tsong, Nano Lett., 2004, 4, 2379–2382.
6. T. Ishikawa, T. Urata, B. Cho, E. Rokuta and C. Oshima, Appl. Phys. Lett., 2007, 90, 143120.
7. W. A. de Heer, A. Charlaid and D. Ugarte, Science, 1995, 270, 1179–1180.
8. Y. Saito, K. Hamaguchi, K. Hata, K. Uchida, Y. Tasaka, F. Ikazaki, M. Yumura, A. Kasuya and Y. Nishina, Nature, 1997, 389, 554–555.
9. G. Zhao, J. Zhang, Q. Zhang, H. Zhang, O. Zhou, L.-C. Qin and J. Tang, Appl. Phys. Lett., 2006, 89, 193113.
10. R. Shimizu, Y. Kataoka, T. Tanaka and S. Kawai, Jpn. J. Appl. Phys., 1975, 14, 1089–1090.
11. M. Futamoto, S. Hosoki, H. Okano and U. Kawabe, J. Appl. Phys., 1977, 48, 3541–3546.
12. S. Zaima, M. Sase, H. Adachi, Y. Shibata, C. Ohshima, T. Tanaka and S. Kawai, J. Phys. D: Appl. Phys., 1980, 13, L47–L49.
13. H. Nagata, K. Harada and R. Shimizu, J. Appl. Phys., 1990, 68, 3614–3618.
14. K. Harada, H. Nagata and R. Shimizu, J. Electron Microsc., 1991, 40, 1–4.
15. M. Nakamoto and K. Fukuda, Appl. Surf. Sci., 2002, 289–294.
16. D. J. Late, M. A. More, D. S. Joag, P. Misra, B. N. Singh and L. M. Kukreja, Appl. Phys. Lett., 2006, 89, 123510.
17. H. Liu, X. Zhang, Y. Li, Y. Xiao, W. Zhang and J. Zhang, Appl. Phys. Lett., 2018, 112, 151604.
18. G. Singh, R. Bucker, G. Kassier, M. Barthelmes, F. Zheng, V. Migunov, M. Kruth, R. E. Dunin-Borkowski, S. T. Purcell and R. J. D. Miller, Appl. Phys. Lett., 2018, 113, 093101.
19. K. Kasuya, T. Kusunoki, T. Hashizume, T. Ohshima, S. Katagiri, Y. Sakai and N. Arai, Appl. Phys. Lett., 2020, 117, 213103.
20. S. Tang, J. Tang, Y. Wu, H. H. Chen, J. Uzuhashi, T. Ohkubo and L. C. Qin, Nanoscale, 2021, 13, 17156–17161.
65 M. Aono, T. Tanaka, E. Bannai, C. Oshima and S. Kawai, *Phys. Rev. B: Solid State*, 1977, **16**, 3489–3492.
66 J. M. Leger, N. Yacoubi and J. Loriers, *J. Solid State Chem.*, 1981, **36**, 261–270.
67 K. Kaminaga, D. Oka, T. Hasegawa and T. Fukumura, *J. Am. Chem. Soc.*, 2018, **140**, 6754–6757.
68 H. Gan, C. Zhang, X. Z. Du, P. Jiang, C. P. Niu, X. H. Zheng, Y. W. Yin and X. G. Li, *Phys. Rev. B*, 2021, **104**, 054515.
69 J. K. Sonber, K. Sairam, T. S. R. C. Murthy, A. Nagaraj, C. Subramanian and R. C. Hubli, *J. Eur. Ceram. Soc.*, 2014, **34**, 1155–1160.
70 H. E. Gallagher, *J. Appl. Phys.*, 1969, **40**, 44–100.
71 T. Mahalingam and M. Radhakrishnan, *J. Mater. Sci. Lett.*, 1986, **5**, 641–642.
72 J. Robertson, *J. Non-Cryst. Solids*, 2002, **303**, 94–100.
73 Y. Kim, S. Ohmi, K. Tsutsui and H. Iwai, *Jpn. J. Appl. Phys.*, 2005, **44**, 4032–4042.
74 I. Rossetto, R. Piagge, F. Toia, S. Spiga, A. Lamperti, S. Vangelista, R. Ritasalo, P. Järvinen and G. Ghidini, *J. Vac. Sci. Technol., B: Nanotechnol. Microelectron.: Mater., Process., Meas., Phenom.*, 2019, **37**, 021205.
75 N. Imanaka, T. Masui and Y. Kato, *J. Solid State Chem.*, 2005, **178**, 395–398.
76 H.-C. Wang, S. Botti and M. A. L. Marques, *npj Comput. Mater.*, 2021, 7, 12.
77 M. A. L. Marques, https://tdff.org/bmg/data.php.
78 J. Ding, Y. Wu, W. Sun and Y. Li, *J. Rare Earths*, 2006, **24**, 440–442.
79 A. Neumann and D. Walter, *Thermochim. Acta*, 2006, **445**, 200–204.
80 R. Nishitani, S. Kawai, H. Iwasaki, S. Nakamura, M. Aono and T. Tanaka, *Surf. Sci.*, 1980, **92**, 191–200.
81 P. R. Davis and S. A. Chambers, *Appl. Surf. Sci.*, 1981, **8**, 197–205.
82 J. S. Ozcomert and M. Trenary, *Chem. Mater.*, 1993, **5**, 1762–1771.
83 C. L. Perkins, M. Trenary, T. Tanaka and S. Otani, *Surf. Sci.*, 1999, **423**, L222–L228.
84 E. Rokuta, N. Yamamoto, Y. Hasegawa, T. Nagao, M. Trenary, C. Oshima and S. Otani, *J. Vac. Sci. Technol., A*, 1996, **14**, 1674–1678.
85 T. Yorisaki, A. Tillekaratne, Y. Moriya, C. Oshima, S. Otani and M. Trenary, *Surf. Sci.*, 2010, **604**, 1202–1207.
86 C.-H. Wen, T.-M. Wu and W.-C. J. Wei, *J. Eur. Ceram. Soc.*, 2004, **24**, 3235–3243.