Research on low-speed characteristics of differential double-drive feed system

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Abstract. It is difficult to achieve high-precision control due to frictional nonlinearity by traditional linear control methodology for the classical drive feed system at low speed. Here, the double-drive differential feed system is proposed to reduce the influence of the nonlinear friction at the ball screw pair of a linear feed system operating at low speed. The dynamic models and the LuGre friction models of the classical drive feed system and the double-drive differential feed system are established, respectively. Based on these, the simulation models of the classical drive feed system and the double-drive differential feed system are established in MATLAB to study the critical creeping velocity of the table. Compared with the classical drive feed system, a lower stable velocity can be obtained for the table with the double-drive differential feed system, because the speed of both motors in the double-drive differential feed system is higher than the critical creeping speed of the classical drive feed system screw motor, thereby overcoming the influence of the Stißeck effect and avoiding the frictional nonlinearity at low speed.

1 Introduction

One of the key technology bottlenecks of ultra-precision machining is how to make the micro-displacement of the tool or workpiece accurate, stable and reliable in the process of machining. The precision drive feed system plays an important role in precision operation such as precision measurement and precision machining (Yung et al., 2003; Kong et al., 2015). However, for the classical drive feed system (CDFS), based on the servo motor and the rolling contact component, it is difficult to achieve precise and uniform motion of the displacement feed because of its low speed and nonlinear crawling problem, which can not meet the urgent needs of ultra-precision machining (Kumar et al., 2012; Chen et al., 2004; Armstrong et al., 1994).

In order to reduce the influence of friction on the feed system, a lot of research has been done on friction modeling and friction compensation (Michael et al., 2004; Shi et al., 2003; Rafael et al., 2019; Naijing et al., 2018; Kai et al., 2018). The LuGre model, put forward by Canudas et al. (1995), includes pre-sliding friction and sliding friction. This model can describe the main characteristics of dynamic friction, including the Stißeck effect, hysteresis, spring characteristics of static friction and changing sliding friction. Liu et al. (2015) proposed a comprehensive identification method for the structure and friction parameters of the ball screw feed system. The distributed component friction model of a feed drive system, which was proposed by Lee et al. (2015), is composed of models of individual feed drive components such as ball screw and linear motion (LM) guide including their friction behaviors. Hongbiao et al. (2009) equated the friction at the linear guide of the ball screw feed system to the rolling friction at the ball screw pair, established a LuGre friction model, and identified the static and dynamic friction parameters of the LuGre friction model. To reduce the influence of friction on the feed system, Lee et al. (2008) proposed a new dual-speed controller for the compensation of nonlinear friction torque, which has an outer speed controller and an inner friction torque compensator. Besides, Han et al. (2012) proposed an adaptive dynamic surface control scheme combined with sliding mode control to compensate for friction and backlash nonlinearities of ball-screw-driven systems.
However, the friction compensation method, based on the friction model proposed above, cannot avoid the nonlinear friction disturbance when the table is running at low speed for the ball screw feed system. In this paper, a novel differential double-drive feed system (DDFS) is developed to minimize the influence of the nonlinear friction at the ball screw pair of a linear feed system operating at low speed. In the DDFS, the screw and the nut are both driven by permanent magnet synchronous motors (PMSMs) that rotate in the same direction at nearly equal high speed, which are superimposed by the ball screw pair to obtain low-velocity linear motion of the table. In this way, it ensures that the driven table travels at low velocity while the two motors are allowed to rotate at high speed. Compared with the CDFS, the DDFS can reduce the influence of the nonlinear friction at the ball screw pair, thereby improving the speed smoothness at low-speed operation.

The remainder of this paper is arranged as follows. The structure of the DDFS is proposed in Sect. 2. The dynamic modeling of the DDFS is described in Sect. 3. The friction model and friction parameter identification are described in Sect. 4. The simulation and analysis of the critical creeping speed of the DDFS are presented in Sect. 5. The experimental results to validate the effectiveness of the proposed method are in Sect. 6. The paper is concluded in Sect. 7.

2 The DDFS description

In the CDFS, the screw shaft is driven by a servo motor through a coupling, and the rotary motion of the motor is converted into the linear motion of the table. The schematic diagram for the structure of the DDFS based on the nut driven ball screw pair is illustrated in Fig. 1.

In the DDFS, the screw shaft and screw nut, both driven by PMSMs, rotate in the same direction at high speed and are superimposed though the ball screw pair to obtain low-velocity linear motion of the table. This design ensures that the driven table travels at low velocity with the two motors rotating at high speed. The low velocity of the table is obtained, and the crawling zone for the motors at low speed is avoided by superimposing two PMSM rotating speeds at high speed by the ball screw pair (Du et al., 2018; Wang et al., 2019). In the DDFS, when the hollow servo motor does not rotate, the DDFS changes to the CDFS.

2.1 The DDFS control strategy

The control strategy of the DDFS is shown in Fig. 2, in which \( x_s, x_n \) and \( x' \) represent the ideal position signal of the screw motor, the ideal position signal of the nut motor and the position measured by grating ruler of the table. To avoid the low-speed crawling area of a single motor, higher speeds for the screw and the hollow motors are given in the DDFS. When the differential table displacement \( x = x_s - x_n \) is required, the differential position signal \( \theta = \theta_s - \theta_n \) is generated by the ball screw pair to drive the table motion. The table position is compared with \( x_t \) after the position feedback through the grating ruler, and the error \( \Delta x = x - x' \) is fed back to the screw motor controller, so the screw motor is adjusted to form a closed-loop control. When the CDFS is used in the DDFS, the table position signal is given to the screw motor, i.e., \( x = x_s \) and the hollow motor position \( x_n = 0 \). Again, the table position is compared with \( x_s \) after the position feedback through the grating ruler, and the error \( \Delta x = x - x_s \) is fed back to the screw motor control, so the screw motor is adjusted to form a closed-loop control.

3 Dynamic modeling of the CDFS and the DDFS

3.1 Dynamic modeling of the CDFS

When the hollow servo motor does not rotate in the DDFS, the dynamic modeling of the CDFS can be illustrated in Fig. 3.

The equation of motion of the CDFS can be described in Eq. (1) (Yu et al., 2016).

\[
\begin{align*}
T_s &= J_s \ddot{\theta}_s + T_{sd} + T_{dd}, \\
T_{sd} &= \frac{p_h}{2 \pi n} F_{sd} = \frac{H}{2} F_{sd}, \\
F_{sd} &= m_{c} \dot{x}_{11} + F_{11}, \\
x_{n1} &= H \theta_s,
\end{align*}
\]

where \( T_s \) is the electromagnetic torque of the screw motor, \( T_{sd} \) is the equivalent friction torque at the screw motor shaft, including the friction torque at the ball screw, the screw support bearing and the screw motor. \( T_{dd} \) is the output torque generated by the interaction between the screw shaft and nut. \( J_s \) is the equivalent moment at the screw motor shaft, including the screw motor shaft, coupling and screw shaft. \( \theta_{ms} \) is the rotation angle of the screw motor. \( \theta_s \) is the rotation angle of the screw shaft. \( F_{sd} \) is the driving force acting on the table. \( F_{11} \) is the friction force at the table. \( x_{11} \) is the axial displacement of the nut. \( p_h \) is the lead of the ball screw, \( \eta \) is the transmission efficiency of the feed system, \( H \) is the screw nut transmission ratio.

The equivalent torsional stiffness \( K_{11} \) of the drive system for the CDFS is shown in Eq. (2) (Wang et al., 2018).

\[
K_{11} = \left( \frac{1}{K_c} + \frac{1}{K_{s\theta}} \right)^{-1}
\]

where \( K_c \) is the torsional stiffness of the coupling, and \( K_{s\theta} \) is the torsional stiffness of the screw shaft.

The equivalent axial stiffness \( K_a \) of the drive system for the CDFS is shown in Eq. (3) (Wang et al., 2018).

\[
K_a = \left( \frac{2}{K_{ba}} + \frac{1}{K_{sa}} + \frac{1}{K_{na}} + \frac{1}{K_{nba}} \right)^{-1}
\]

where \( K_{ba} \) is the axial stiffness of the bearing, \( K_{sa} \) is the axial stiffness of the screw shaft, \( K_{na} \) is the axial stiffness of the nut and \( K_{nba} \) is the axial stiffness of the nut bearing.
The axial rigidity of the screw is shown in Eq. (4) (Wang et al., 2018):

\[ K_{sa} = \frac{\pi d^2 E l}{4a(l - a)} \]  

where \( E \) is the elastic modulus of the screw shaft, \( d \) is the diameter of the screw shaft, \( l \) is the span between the screw supports and \( a \) is the distance from the action point to the support.

The comprehensive equivalent stiffness of the DDFS is shown in Eq. (5) (Yu et al., 2016).

\[ K_{eq} = \left( \frac{1}{K_a} + \frac{H^2}{\eta} \cdot \frac{1}{K_{t1}} \right)^{-1} \]  

The axial displacement \( x_{t1} \) of the table can be expressed as shown in Eq. (6) (Wang et al., 2018).

\[ x_{t1} = H \theta_{ms} - F_{sd}/K_{eq} \]  

3.2 Dynamic modeling of the DDFS

The dynamic modeling of the DDFS can be illustrated in Fig. 4.
It is assumed that the rotation angle of the screw motor is larger than that of the hollow motor, and the torsional deformation between the screw motor and the screw shaft is ignored at the same time. The equation of motion of the DDFS can be described by Eq. (7) (Wang et al., 2019).

\[
\begin{align*}
T_s - T_{sf} - T_d &= J_s \ddot{\theta}_s, \\
T_n - T_{nf} + T_d &= J_n \ddot{\theta}_n,
\end{align*}
\]

(7)

where \( T_s \) is the electromagnetic torque of the hollow motor, \( T_{sf} \) is the friction torque equivalent to the hollow motor shaft, \( T_d \) is the friction torque at the screw motor shaft and \( \theta_s \) is the rotation angle of the screw motor. \( T_d \) is the output torque generated by the interaction between the screw shaft and nut. \( J_n \) is the moment of inertia equivalent to the hollow motor shaft, including the hollow motor shaft, screw nut and connecting flange. \( \theta_n \) is the rotation angle of the screw nut.

Eq. (8) can be obtained by the motion analysis of the table (Wang et al., 2019).

\[
\begin{align*}
F_d &= K_{eq} [H (\theta_s - \theta_n) - x], \\
F_d - F_t &= m_i \ddot{x}_t, \\
T_d &= F_d H, \\
H &= \frac{F_d}{2\pi},
\end{align*}
\]

(8)

4 Friction modeling of the DDFS

In the DDFS, friction can be subdivided into the following three parts: friction torque equivalent to the screw motor shaft, including the friction torque at the screw motor bearing, the screw support bearing, and the ball screw; the friction torque equivalent to the hollow motor shaft, including the friction torque of the hollow motor bearing and the nut bearing; and the friction force at the table.

4.1 Friction modeling of the screw motor shaft

The friction modeling of the screw motor shaft is shown in Eq. (9) (Du et al., 2018).

\[
\begin{align*}
T_{sf} &= \sigma_{0s} z_s + \sigma_{1s} \dot{z}_s + \sigma_{2s} \dot{\theta}_s, \\
\dot{z}_s &= \dot{\theta}_s - \frac{[\dot{\theta}_s]}{[g(\theta_s)]} z_s, \\
[\sigma_{0s} g(\dot{\theta}_s)] &= T_{scr} + (T_{ns} - T_{ncr})e^{-\frac{\sigma_{1s} z_s}{[g(\theta_s)]}},
\end{align*}
\]

(9)

where \( T_{sf} \) is the friction torque equivalent to the screw motor shaft, \( \sigma_{0s} \) is the stiffness coefficient of the screw motor shaft, \( \sigma_{1s} \) is the damping coefficient of the screw motor shaft, \( \sigma_{2s} \) is the viscous friction coefficient of the screw motor shaft, \( T_{ns} \) is the maximum static friction torque of the screw motor shaft, \( T_{ncr} \) is the Coulomb friction torque of the screw motor shaft and \( \sigma_{1s} \) is the Stribeck velocity of the screw motor shaft.

4.2 Friction modeling of the hollow motor shaft

The friction modeling of the hollow motor shaft is shown in Eq. (10) (Du et al., 2018).

\[
\begin{align*}
T_{nf} &= \sigma_{0n} z_n + \sigma_{1n} \dot{z}_n + \sigma_{2n} \dot{\theta}_n, \\
\dot{z}_n &= \dot{\theta}_n - \frac{[\dot{\theta}_n]}{[g(\theta_n)]} z_n, \\
[\sigma_{0n} g(\dot{\theta}_n)] &= T_{ncr} + (T_{ns} - T_{ncr})e^{-\frac{\sigma_{1n} z_n}{[g(\theta_n)]}},
\end{align*}
\]

(10)

where \( T_{nf} \) is the friction torque equivalent to the hollow motor shaft, \( \sigma_{0n} \) is the stiffness coefficient of the hollow motor shaft, \( \sigma_{1n} \) is the damping coefficient of the hollow motor shaft, \( \sigma_{2n} \) is the viscous friction coefficient of the hollow motor shaft, \( T_{ns} \) is the maximum static friction torque of the hollow motor shaft, \( T_{ncr} \) is the Coulomb friction torque of the hollow motor shaft and \( \sigma_{1n} \) is the Stribeck velocity of the hollow motor shaft.

4.3 Friction modeling of the linear guide

The friction modeling of the linear guide is shown in Eq. (11) (Du et al., 2018).

\[
\begin{align*}
F_{lg} &= \sigma_{0l} z_l + \sigma_{1l} \dot{z}_l + \sigma_{2l} \dot{\theta}_l, \\
\dot{z}_l &= \dot{\theta}_l - \frac{[\dot{\theta}_l]}{[g(z_l)]} z_l, \\
[\sigma_{0l} g(\dot{\theta}_l)] &= F_{lc} + (F_{ls} - F_{lc})e^{-\frac{\sigma_{1l} z_l}{[g(z_l)]}},
\end{align*}
\]

(11)

where \( F_{lg} \) is the equivalent friction force at the linear guide, \( \sigma_{0l} \) is the stiffness coefficient of the linear guide, \( \sigma_{1l} \) is the damping coefficient of the linear guide, \( \sigma_{2l} \) is the viscous friction coefficient of the linear guide, \( F_{ls} \) is the maximum
Table 1. Friction parameters in the DDFS.

| Friction parameter | The screw motor shaft | The hollow motor shaft | Linear guide |
|--------------------|-----------------------|------------------------|--------------|
|                    | Positive | Negative | Positive | Negative | Positive | Negative |
| $F_c$ (N)          | 73.4     | -68.5     | 76.2     | -72.1     | 14.7     | -14.3    |
| $F_s$ (N)          | 96.4     | -94.6     | 108.4    | -102.3    | 22.5     | -22.9    |
| $v_s$ (m s$^{-1}$) | $8.64 \times 10^{-4}$ | $-9.01 \times 10^{-4}$ | $9.38 \times 10^{-4}$ | $-9.56 \times 10^{-4}$ | $1.45 \times 10^{-3}$ | $-1.36 \times 10^{-3}$ |
| $\sigma_2$ (N m$^{-1}$) | $3.14 \times 10^3$ | $2.76 \times 10^3$ | $3.12 \times 10^3$ | $3.01 \times 10^3$ | 61.6     | 62.3      |
| $\sigma_0$ (N m$^{-1}$) | $3.64 \times 10^7$ | $3.61 \times 10^5$ | $4.38 \times 10^5$ | $4.38 \times 10^5$ | $4.38 \times 10^5$ | $4.38 \times 10^5$ |
| $\sigma_1$ (N m$^{-1}$) | $5.26 \times 10^3$ | $5.76 \times 10^3$ | $1.86 \times 10^3$ | $1.86 \times 10^3$ | $1.86 \times 10^3$ | $1.86 \times 10^3$ |

Figure 5. Block diagrams of the CDFS (a) and the DDFS (b).

5 Simulation and analysis of critical creeping speed of the DDFS

5.1 The simulation platform of the DDFS

The simulation models of the CDFS and the DDFS are established in MATLAB according to the established dynamic and friction models. To compare and study the critical creeping speed of the table by using different driving methods, we set the same control parameters for the two motors. Figure 5a and b are the CDFS and DDFS control block diagrams established in MATLAB/Simulink. The parameters of the DDFS are shown in Table 2.
Table 2. Parameters in the DDFS.

| Parameters                                      | Values                  |
|------------------------------------------------|-------------------------|
| Length of the screw shaft, $l$ (mm)            | 800                     |
| Diameter of the screw shaft, $d$ (mm)          | 16                      |
| Helical pitch of the screw shaft, $p_h$ (mm)   | 5                       |
| Torsional stiffness of the screw shaft, $k_\text{eq}$ (N m rad$^{-1}$) | 61 368                  |
| Axial stiffness of the screw-shaft, $k_{\text{na}}$ (N m$^{-1}$) | $2.48 \times 10^8$      |
| Axial stiffness of the bearing of the screw nut, $k_{\text{nba}}$ (N m$^{-1}$) | $3.12 \times 10^8$      |
| Axial stiffness of the supporting bearing of the ball screw, $k_{\text{ha}}$ (N m$^{-1}$) | $1.06 \times 10^8$      |
| Torsional stiffness of the coupling, $k_c$ (N m rad$^{-1}$) | $2.81 \times 10^4$      |
| Position loop gain, $K_{\text{pp}}$            | 8                       |
| Velocity-adjusting gain, $K_{v}$ (rad (V s)$^{-1}$) | 250                     |
| Velocity loop gain, $K_{\text{vp}}$ (A s rad$^{-1}$) | 45                      |
| Current loop gain, $K_{ip}$ (V A$^{-1}$)       | 2                       |
| Motor torque constant, $K_t$ (Nm A$^{-1}$)     | 0.55                    |
| Motor back electromotive force coefficient, $K_{\text{emf}}$ (V s rad$^{-1}$) | 0.15                    |
| Motor armature inductance, $L$ (mH)            | 5.9                     |
| Motor armature resistance, $R$ ($\Omega$)      | 1.7                     |
| Moment of inertia of the motor, $J_s$, $J_n$ (kg m$^2$) | $1.38 \times 10^3$      |
| Mass of the table, $m_t$ (kg)                  | 20                      |

Figure 6. The speed of the table at different speeds for the CDFS.

5.2 Constant speed analysis of the table in the middle of the screw shaft

$K_{\text{eq}}$ is $2.16 \times 10^7$ N m$^{-1}$, when the table is in the middle of the screw shaft. Figure 6 shows the velocity of the table at different velocities for the CDFS. Figure 6a shows that the table crawls at 1.55 mm s$^{-1}$ for the CDFS. This is because the command velocity of the table is lower than the Striebeck velocity of the table. Figure 6b shows that the velocity of the table has stabilized at 1.56 mm s$^{-1}$ after 7 s of adjustment time for the CDFS. Therefore, the critical creeping velocity of the table is about 1.56 mm s$^{-1}$ for the CDFS.

Figure 7 shows the speed of the table at 1.55 mm s$^{-1}$, when the selected different speeds of the two motors are superimposed at the ball screw pair for the DDFS. The hollow motor keeps a constant speed $v_h$ all the time in Fig. 7. In order to avoid low-speed crawling of the CDFS, the speed of both motors in the DDFS is selected to be greater than the critical crawl speed of the CDFS (1.56 mm s$^{-1}$).

Figure 7 shows that when the velocity of the table is 1.55 mm s$^{-1}$, the velocity overshoot and adjustment time of the table during the acceleration stage gradually decrease as the speed of the hollow motor increases. Figure 7 shows that when the speed of the hollow motor is greater than 10 times the critical creeping speed of the CDFS, there is almost no significant change in the acceleration stage velocity and adjustment time of the table for the DDFS. Therefore, the speed of the hollow motor should be 10 times greater than the critical creeping speed of the CDFS to obtain a stable table velocity in the DDFS.
The speed of the two motors in the DDFS is 10 times greater than the critical creeping speed of the screw servo motor of the CDFS. The obtained critical creeping speed of the table is $0.5 \text{ mm s}^{-1}$ for the DDFS, as shown in Fig. 8.

Figure 6 indicates that the velocity of the table at $1.55 \text{ mm s}^{-1}$ has a serious creep phenomenon in the CDFS, because the friction of the ball screw pair at low speed is in the pre-sliding friction zone. Figures 7 to 8 indicate that a lower stable velocity of the table is achieved for the DDFS compared with the CDFS, because the speed of both motors in the DDFS is higher than the critical creeping velocity of the CDFS. The two motors work in a relatively higher speed in the DDFS, which overcomes the influence of the Stribeck effect at low speed and avoids the frictional nonlinearity at low speed compared with the CDFS.

5.3 Variable speed analysis of the table in the middle of the screw shaft

To research the speed overshoot of the table under the sinusoidal speed signal for the DDFS compared with the CDFS, the table speed is set to $1.56$ and $2 \text{ mm s}^{-1}$, respectively,
which is greater than the critical creeping speed of the table (1.56 mm s\(^{-1}\)) for the CDFS. Figures 9 and 10 show the speed of the table for the CDFS compared with the DDFS in which the selected different speed amplitudes of the two motors are superimposed at the ball screw pair for the DDFS. In Figs. 9 and 10, \(v_{sp}, v_{np}\) and \(v_{tp}\) represent the sine speed amplitudes of the screw motor, hollow motor and table, respectively.

Figure 10b–d indicate that as the speed amplitude of the hollow motor increases, the overshoot of the table during speed reversal gradually decreases. Comparing with Fig. 10a, Fig. 10d indicates that the speed of the table only has a more obvious overshoot at the zero crossing for the DDFS when the amplitude speed of the hollow motor is 10 times greater than the critical creeping speed of the screw servo motor for the CDFS. Under the sinusoidal speed signal, the better speed tracking performance of the table is obtained for the DDFS compared with the CDFS.

6 Experiment of the critical creep velocity of the table in the CDFS and in the DDFS

To verify the accuracy of the modeling of the DDFS, the critical creeping speed of different driving modes was measured when the table was fed at a low speed. The critical creeping speed test of the DDFS is shown in Fig. 11.

The simulation in Sect. 5 indicates that the speed of the hollow motor should be 10 times greater than the critical creeping speed of the CDFS to obtain a stable table speed in the DDFS. Therefore, the speed of the hollow motor \(v_h\) is set to 20 mm s\(^{-1}\) in the DDFS for the experimental tests. The measured direct-drive servo system travel is 400 mm. A total of five measurement points are taken in the test. The Renishaw XL laser interferometer is used to measure the critical creeping speed of the DDFS compared with the CDFS, as shown in Fig. 12.

At each measurement point, a machine tool control program makes the table move uniformly along the axis. The table starts with a higher velocity, and we use a Renishaw XL laser interferometer to measure the dynamic response of the table. Then, we observe the table for crawling behavior. If no crawling occurs, we reset the velocity of the table and reduce the velocity in steps of 0.01 mm s\(^{-1}\) until it is found that the table is crawling. We record the position of the measurement point and the data of the critical creeping speed in turn. Since the relative displacement of the table is small, the measured critical crawling velocity can be regarded as the critical creeping velocity of the table at this measuring point.
Figure 10. The speed of the table is 2 mm s\(^{-1}\).

Figure 11. Critical creeping velocity test of the DDFS and the CDFS.

Figure 12. Measurement points.

The critical creeping velocity of the table at measurement point 3 in the CDFS and the DDFS is shown in Fig. 13. Figure 13a and b show that the critical creeping speed of the table for the experiment is 1.66 mm s\(^{-1}\) in the CDFS. Figure 13c and d show that the critical creeping speed of the table for the experiment is 0.52 mm s\(^{-1}\) in the DDFS when the speed of the hollow motor \(v_a\) is set to 20 mm s\(^{-1}\) in the DDFS.

After repeated measurements, the critical creeping velocity of the table at each measurement point in the DDFS and the CDFS is shown in Table 3. The relationship among the critical creeping velocity of the table, the axial stiffness of the ball screw, and the position of the table of the DDFS and the CDFS is shown in Fig. 14.
Figure 13. The critical creeping velocity at measurement point 3 of the table.

Table 3. Critical creeping velocity of the table for the DDFS compared with the CDFS.

| Parameters                                                   | Measurement points |
|--------------------------------------------------------------|--------------------|
| Position of the table, \(x\) (mm)                          | 200 300 400 500 600 |
| Axial stiffness of the ball screw, \(k_{sa}\) (Nµm\(^{-1}\)) | 276.13 220.9 207.1 220.9 276.13 |
| Critical creeping velocity of the table for the CDFS, \(v\) (mm s\(^{-1}\)) | 1.21 1.58 1.66 1.59 1.23 |
| Critical creeping velocity of the table for the DDFS, \(v\) (mm s\(^{-1}\)) | 0.35 0.47 0.52 0.46 0.36 |

Figure 6 shows that the critical creeping speed of the table is about 1.56 mm s\(^{-1}\) for the CDFS in numerical simulations. Table 3 and Fig. 14 show that the critical creeping speed of the table for the experiment is 1.66 mm s\(^{-1}\) in the CDFS. The difference is caused by the manufacturing error of the ball screw pair, the error of the identified friction parameters and the error of the system stiffness value. Table 3 and Fig. 14 show that the critical creep velocity for the table decreased from 1.66 mm s\(^{-1}\) with the CDFS to 0.52 mm s\(^{-1}\) with the DDFS, when the table is in the middle position of the screw shaft. At the same measurement point, a lower critical creep velocity of the table is achieved for the DDFS compared with the CDFS. At the same time, it can be found that the critical creep velocity of the table at the five measuring points is different, and the critical creep velocity is greater as it approaches the middle position of the screw shaft. The friction conditions and control parameters at the five measuring points are consistent. Therefore, the critical creeping speed of the table is related to the axial rigidity of the ball screw shaft. The greater the axial rigidity of the ball screw, the lower the critical crawl speed of the table.

7 Conclusions

In this paper, the DDFS is developed to reduce the influence of the nonlinear friction at the ball screw pair of a linear feed system operating at low speeds, and some conclusions are drawn as follows.
1. The dynamic models of the CDFS and the DDFS are established. In the DDFS, friction can be subdivided into the following three parts: friction torque equivalent to the screw motor shaft, the friction torque equivalent to the hollow motor shaft and the friction force of the linear guides. The LuGre friction model is adopted as the friction model.

2. Compared with the CDFS, a lower stable speed of the table is achieved in the DDFS, because the speed of both motors in the DDFS is higher than the critical creeping speed of the CDFS. The two motors work at a relatively higher speed in the DDFS, which overcomes the influence of the Stribeck effect at low speed and avoids the frictional nonlinearity at low speed. The speed of the hollow motor should be 10 times greater than the critical creeping speed of the CDFS to obtain a stable table speed in the DDFS.

3. The critical creeping speed of the table is related to the axial rigidity of the ball screw shaft. And the greater the axial rigidity of the ball screw, the lower the critical creeping velocity of the table.

Data availability. All data included in this study are available upon request by contacting the corresponding author.

Author contributions. ZW made substantial contributions to the conception and design, the acquisition, the analysis, and the interpretation of data for the work. He also drafted the work and revised it critically for important intellectual content. ZW made a contribution to the acquisition of simulation experimental data and data collation. XF supervised and structured the process of the paper. HY helped with making figures. HJ helped with the writing and language.

Competing interests. The authors declare that they have no conflict of interest.

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