Impact of mixing intensity on dissolved oxygen half-velocity constants in a sidestream deammonification environment
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ABSTRACT
A partial nitritation/anammox (PN/A) process was operated at two different mixing intensities to quantify the extent to which diffusional limitations impact process rates. At a steady-state operation, the total inorganic nitrogen removal efficiency in the bench-scale sequencing batch reactors was found to increase as mixing intensity decreased (62 and 84% for average velocity gradient ($G$) values of 15 and 5.3 s$^{-1}$, respectively). The half-velocity constants ($K_{O2}$) with respect to bulk-phase dissolved oxygen (DO) concentration for ammonia-oxidizing bacteria (AOB) and anaerobic ammonium-oxidizing (anammox) organisms were estimated on the basis of nitrogen removal rates that were observed in activity tests. The activity tests were conducted over a range of bulk-phase DO concentrations. The best-fit $K_{O2}^{AOB}$ values were estimated to be $0.68 \pm 0.34$ and $0.54 \pm 0.56$ mg O$_2$/L for $G$ values of 15 and 5.3 s$^{-1}$, respectively. The AOB values were not statistically different ($p = 0.19$) between mixing conditions which were consistent with AOB dominating the surface of granules. The best-fit $K_{O2}^{anammox}$ values were estimated to be $0.13 \pm 0.09$ and $0.55 \pm 0.40$ mg O$_2$/L for $G$ values of 15 and 5.3 s$^{-1}$, respectively, and were statistically different ($p = 3.9 \times 10^{-10}$). The results demonstrated that mixing conditions should be considered when designing PN/A processes and provide quantitative results that can be employed to improve models of these processes.

Key words | anaerobic ammonium oxidation, anammox, half velocity, model, nitrogen, short-cut nitrogen

INTRODUCTION
There is a growing interest in the use of short-cut nitrogen removal processes that remove nitrogen from wastewater streams with fewer resources (energy and carbon) than traditional technologies (Kartal et al. 2010). Lackner et al. (2014) reported 100 full-scale installations of technologies that employ partial nitritation and anammox (PN/A) for nitrogen removal. PN/A processes oxidize a portion of ammonia to nitrite with ammonia-oxidizing bacteria (AOB) in the presence of dissolved oxygen (DO), while ammonium and nitrite are removed by anammox bacteria in zones where DO is depleted (Van Hulle et al. 2010). The successful operation of PN/A processes typically depends on establishing conditions (including low DO concentrations) that result in the wash-out of nitrite-oxidizing bacteria (NOB) from the process. The DO profile is critical to successful operations and is typically controlled by setting the duration of aerated and unaerated periods and the target DO concentration while aerating (Lackner et al. 2015).

The successful operation of PN/A processes typically requires the implementation of sophisticated pH and DO
control on aeration (Wett 2007; Wett et al. 2007). There is, however, a lack of consensus with regard to the target DO concentration that should be employed during aeration. Lackner et al. (2014) reported target DO concentrations that ranged from 0.3 to 1.5 mg O$_2$/L. The matter is further complicated by the fact that some technologies utilize intermittent aeration, while others utilize continuous aeration (Lackner et al. 2014; Corbalá-Robles et al. 2016).

Process modeling can be employed to inform decisions regarding process operation and control. Mechanistic models employ switching functions which incorporate half-velocity constants ($K_{O_2}$) to describe the impact of DO concentration on the growth of AOB, NOB, and anammox organisms (Vangsgaard et al. 2015; Ni et al. 2014; Corbalá-Robles et al. 2016). Historically, the models have assumed that all organisms are directly exposed to the bulk liquid substrate concentrations, and the half-velocity coefficients (referred to as intrinsic) have been considered to be constant. However, recent studies have shown that the values of substrate half-velocity constants should be considered as variables (Arnaldos et al. 2015; Ma et al. 2016) with values having substantial ranges (i.e. 33-fold variation of reported $K_{O_2}$ values for AOB). Limitations in oxygen availability in the interior of floc and granules that are imposed by advection and diffusion have been hypothesized to be responsible for differences in half-velocity constants. The observed values should be considered as extant (Arnaldos et al. 2015). While floc-based models that incorporate diffusional resistances have been developed, they are difficult to apply due to the uncertainty in many variables (Shaw et al. 2015). There is a need to have information that describes how extant half-velocity values vary as a function of factors that impact upon diffusive processes.

Previous studies have focused on factors that influenced diffusive limitations in systems that included AOB and NOB. Mixing intensity has been reported to influence both advection and diffusion in floc. Chu et al. (2005) reported that $K_{O_2}$ values increased as mixing intensity decreased when activated sludge was tested in a respirometer. Furthermore, Wu et al. (2007) found that $K_{O_2}$ values increased with increased floc size and nitrifier density inside flocs. While these studies demonstrate the impact of mixing intensity on $K_{O_2}$, there is less information on PN/A granules that rely on organisms with opposing DO sensitivities and which are operated to optimize DO gradients within the granules.

This study focused on the impact of mixing intensity on the observed extant half-velocity constants of AOB ($K_{O_2}^{AOB}$) and anammox bacteria ($K_{O_2}^{anammox}$) values in a PN/A process environment. It was hypothesized that the AOB activity would increase with mixing intensity since it would depend on the availability of both NH$_4^+$ and oxygen to the organisms, and both of these would increase with improved mass transfer. By contrast, the anammox activity is reduced in the presence of DO and, therefore, may increase under conditions of reduced mass transfer. $K_{O_2}$ values were estimated by modeling data that were generated in a PN/A reactor when it was operated in a batch mode. The batch tests facilitated the calculation of substrate utilization rates for ammonium, nitrite, and nitrate under different DO concentrations. The estimated $K_{O_2}$ values provide wastewater treatment practitioners with insights into the impact of mixing intensity on process rates and ultimately with establishing target bulk liquid DO concentrations when aerating PN/A reactors.

**METHODOLOGY**

**Experimental plan**

A bench-scale sequencing batch reactor (SBR) was operated to generate data that were subsequently employed to assess the impact of mixing intensity on the rates of substrate utilization. It was operated for an extended period of time at two different mixing intensities to facilitate an assessment of the impact of mixing intensity on the performance of the reactor and the $K_{O_2}^{AOB}$ and $K_{O_2}^{anammox}$ values. In the initial phase of testing, the mixer was operated at 150 rpm (an equivalent of the average velocity gradient ($G_{150 \text{ rpm}}$) of 15 s$^{-1}$); while in the second phase of testing, a rotational velocity of 75 rpm (an equivalent ($G_{75 \text{ rpm}}$) of 5.3 s$^{-1}$) was employed to span a range of values. After steady-state conditions were established at each mixing intensity, the operational mode of the SBR was switched to the batch mode to conduct a series of activity tests that generated data which was employed to estimate $K_{O_2}^{AOB}$ and $K_{O_2}^{anammox}$ values. The activity tests incorporated anoxic and aerobic conditions as are described in detail subsequently.

The goal was to conduct activity tests with the granule morphology that was established through the long-term
operation at each mixing intensity. Given the considerable period of time required to complete each phase, resource limitations resulted in the testing of two mixing conditions that spanned a range of intensities. The results of the study facilitated an assessment of which half-velocity parameters were sensitive to mixing intensity. Additional research would be required to develop quantitative relationships between mixing intensity and half-velocity constant values.

**Test apparatus**

The SBR had an effective volume of 8.0 L, was heated to maintain a temperature of 35 °C, and received diffused air (Bubble Mist, Woodbridge, ON, Canada) provided by an air pump (Elite Optima, Model #A-807, Rolf C. Hagen Inc., Baie d’Urfé, QC, Canada). The reactor was mixed with a 120 mm diameter vertical-flat-blade impeller. The SBR was operated at a hydraulic retention time (HRT) of 12 h with two cycles per HRT. Each cycle consisted of the initial 330 min of continuous feeding (13 mL/min), aerating, and mixing, and this was followed by 20 min of settling and 10 min of decanting. DEMON® biomass from the York River Treatment Plant located in Seafood, VA, USA was used as the inoculum to initiate the SBR operations.

The SBR aeration strategy was adopted from literature reports (Wett 2006; Wett et al. 2007; Jardin & Hennerkes 2012) and employed continuous monitoring of pH and DO to inform a control algorithm that was designed to achieve the PN/A activity. The air-flow settings were adjusted at the outset of the testing, such that the controller could maintain DO in the target range without significant fluctuations. During feeding and mixing, the SBR was intermittently aerated at a flow rate of 5.5–6.5 L/min (Wett et al. 1998) on and off for periods of 6 and 3 min, respectively. Aeration was paused either when the DO exceeded 0.80 mg O2/L or the pH decreased below 7.0. In situations when the pH became less than 7.0, the aeration resumed upon the commencement of the subsequent aeration period when the pH increased above 7.0.

Selective wasting of biomass was employed to minimize the NOB population in the SBR. The selective wasting procedure (Wett et al. 2010, 2013, 2015) involved transferring 300 mL of wasted mixed liquor suspended solids (MLSS) (collected at the end of each SBR cycle) to a separatory funnel, swirling the funnel for 15 s, and then allowing the solids to settle. As the supernatant became clear, the stopcock was opened and granular biomass was collected from the stem at the bottom. The stopcock was closed when the solids surface level reached approximately 66% of the solids blanket depth. These solids were returned to the reactor, while the remaining biomass that was more flocculent in nature was wasted. In this way, the solids retention time (SRT) for low-density floc and high-density granules were decoupled.

The range of SRT for the flocs and granules was estimated on the basis of two different assumptions regarding

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**Table 1** | Composition of synthetic centrate

| Component            | Concentration          |
|----------------------|------------------------|
| NH₄HCO₃              | 2,820 mg/L (500 mg/L as N) |
| NaHCO₃               | 420 mg/L (250 mg/L as CaCO₃) |
| KH₂PO₄               | 27.2 mg/L               |
| MgSO₄                | 147 mg/L                |
| CaCl₂ · 2H₂O         | 180 mg/L                |
| Trace element I      | 1 mL/L of synthetic centrate |
| Trace element II     | 1 mL/L of synthetic centrate |
the separation of the floc and granules in the separatory funnel. One scenario assumed that the selective wasting method achieved no biomass separation and the SRTs for the floc and granules were the same, with a value of 22.5 days. The alternate scenario assumed that the selective wasting method achieved perfect separation where all granules were recycled and at the same time all flocs were wasted. In this scenario, the floc SRT was 6.7 d and the granule SRT approached infinity. It is believed that the actual SRT values were between the extremes.

**Batch activity tests**

The batch activity tests were conducted upon the completion of an SBR feeding and mixing cycle and employed procedures that have been previously reported (Tsushima et al. 2007; Williams et al. 2012; Nifong et al. 2015). Each test involved an initial anoxic phase with a 1 h duration where granular NH₄HCO₃ (an equivalent of 50 mg N L⁻¹) and NaNO₂ (an equivalent of 75 mg N L⁻¹) were added to the reactor and the DO concentration was maintained below detection limits (0.07 mg/L). These dosages were expected to saturate the relevant substrate switching functions based on half-velocity values that were obtained from the literature (Vangsgaard et al. 2013; Ni et al. 2014; Corbalá-Robles et al. 2016).

Upon the completion of the anoxic phase, aerobic conditions were established at targeted DO concentrations, and granular NH₄HCO₃ (an equivalent of 200 mg N L⁻¹) was added to the SBR and the test continued for an hour. The aerobic tests were conducted at different DO concentrations that ranged from 0.25 to 6.42 mg O₂/L at G₁50 rpm and 0.59 to 5.84 mg O₂/L at G₇5 rpm. A total of nine tests at G₁50 rpm and six tests at G₇5 rpm were conducted, and the tests with target DO concentrations of 4.0 and 6.0 mg O₂/L were replicated twice at G₁50 rpm. Typically, five to six samples were collected over the 1 h duration of both the anoxic and aerobic activity phases to measure NH₄⁺, NO₂⁻, and NO₃⁻ concentrations. The sampling frequency was increased for the first 15 min of the tests (0, 7.5, and 15 min) when responses were expected to be more rapid and was then reduced to 15-min intervals for the remainder of the test. At the end of the aerobic phase, the reactor contents were analyzed for total suspended solids (TSSs) and volatile suspended solids (VSSs) to establish the MLSS.

**Analytical methods**

The concentrations of TSSs, VSSs, NH₄⁺, NO₂⁻, and NO₃⁻ were measured according to Standard Methods (American Public Health Association 2005). Ammonium (NH₄⁺) concentrations were measured by an ion-selective electrode (ISE) (Orion™ High Performance Ammonia ISE, 9512HPBNWP, Thermo Fisher Scientific, Sunnyvale, CA, USA). Nitrite (NO₂⁻) and nitrate (NO₃⁻) were measured by ion chromatography (Dionex IonPac™ AS4A-SC, Thermo Fisher Scientific, Sunnyvale, CA, USA).

**Statistical methods**

Multi-response regression was used to calibrate the DO half-velocity constants in the bioprocess model (Ni et al. 2014) that was adopted in this study. Two-sample t-tests (significance level of 0.05) were used to determine whether the DO half-velocity constants differed between the two mixing intensities.

**RESULTS AND DISCUSSION**

The testing was divided into two phases where the mixer was operated at different speeds and mixing intensities (G₁50 rpm and G₇5 rpm, respectively). Achieving steady state with respect to the activity of the biomass in the reactor was deemed to be important in terms of increasing the accuracy of the subsequent batch activity testing and the confidence in the estimation of the Kₐ. The SBR was therefore operated until steady state was achieved prior to the batch activity tests. Steady-state conditions were assessed based on the presence of stable effluent concentrations of NH₄⁺, NO₂⁻, and NO₃⁻ over time (Figure 1). Steady state was deemed to be achieved for days 81–165 and 199–228 in Phases 1 and 2, respectively. The average (±std dev) MLVSS concentrations at steady state were 1.2 ± 0.35 and 1.9 ± 0.09 g/L in Phases 1 and 2, respectively.

Comparing Phases 1 and 2, the average effluent NH₄⁺ concentration in Phase 2 decreased to approximately 35%...
of that observed in Phase 1. The effluent concentrations of NO$_2^-$ were negligible throughout the steady-state periods, while the average effluent NO$_3^-$ concentration decreased only slightly in Phase 2 as compared to Phase 1. The total inorganic nitrogen (TIN) removal efficiency was calculated for the steady-state periods with values of 62 and 84% for Phases 1 and 2, respectively.

The results indicate that the largest contribution to the increased TIN removal with reduced mixing intensity was the increased removal of NH$_4^+$ which could be attributed to increase the activity of either AOB or anammox. It was hypothesized that the AOB activity would increase with mixing intensity since it would depend on the availability of both NH$_4^+$ and oxygen to the organisms and both of these would increase with improved mass transfer. By contrast, the anammox activity is reduced in the presence of DO and therefore may increase under conditions of reduced mass transfer. It was not possible to confirm these hypotheses with the data obtained from the continuous operation of the SBR, and the subsequently described batch testing and model application were conducted to investigate the impact of mixing on AOB and anammox activity in more depth.

The activity tests were conducted with the SBR operating in the batch mode and with known initial concentrations of NH$_4^+$, NO$_2^-$, and NO$_3^-$. Each consisted of anoxic and aerobic periods with the DO concentration in the latter period differing between tests. Trends in substrate concentrations with time were employed to determine substrate utilization rates that were subsequently used to estimate the $K_{AOB}^{O_2}$ and $K_{anammox}^{O_2}$ values.

The concentrations of NH$_4^+$, NO$_2^-$, and NO$_3^-$ at G$_{150}$ rpm that were observed in a test that was conducted in Phase 1, when the DO concentration in the aerobic portion of the test was 0.46 mg O$_2$/L, are shown in Figure 2 and are representatives of those obtained under other test conditions. From Figure 2, it can be seen that the concentration of NH$_4^+$ initially increased and then decreased linearly in both the anoxic and aerobic conditions. The early increase in the NH$_4^+$ concentrations was attributed to the time required to dissolve and mix the dry substrates that were added to the reactor. Only the concentration profiles obtained after 15 min were used for further analysis of conversion rates.

The trends in substrate responses in the batch tests were consistent with the metabolisms that were anticipated to be active in the different aeration conditions. Under anoxic conditions, NH$_4^+$ and NO$_2^-$ concentrations decreased and NO$_3^-$ increased over time. These responses were observed in all of the anoxic tests and were attributed to the activity
of anammox organisms. Under aerobic conditions, the \( \mathrm{NH}_4^+ \) concentrations decreased, while \( \mathrm{NO}_3^- \) concentrations increased in all tests. By contrast, \( \mathrm{NO}_2^- \) concentrations declined with time in tests conducted when the DO was in the range of 0.5 mg/L (as observed in Figure 2) but increased with time in tests with higher DO concentrations. The results obtained under the aerobic conditions were somewhat inconsistent with predictions based on DO half-velocity constants reported in the literature (Vangsgaard et al. 2013; Ni et al. 2014; Corbalá-Robles et al. 2016) where values of 0.01 mg O2/L have been reported for anammox organisms. With DO concentrations of 0.5 mg O2/L in the bulk liquid, it was anticipated that \( \mathrm{NO}_2^- \) would not be removed in the system as the anammox activity would be inhibited. The \( \mathrm{NO}_2^- \) removal that was observed in the 0.5 mg O2/L aerobic conditions under both mixing conditions suggested the presence of anoxic zones within the granule structures.

Figure 3 presents the net rates of \( \mathrm{NH}_4^+ \), \( \mathrm{NO}_2^- \), and \( \mathrm{NO}_3^- \) conversion versus DO concentration that were observed in the batch tests for both phases. These rates were calculated based on the slopes of the nitrogen species concentration responses that were generated in the aerobic batch tests. A positive value for the rate was interpreted to indicate that the production rate of the species was greater than the consumption rate, while a negative value indicated that the production rate was less than the consumption rate.

The \( \mathrm{NH}_4^+ \), \( \mathrm{NO}_2^- \), and \( \mathrm{NO}_3^- \) conversion rates under anoxic conditions at both \( G_{75 \text{ rpm}} \) and \( G_{150 \text{ rpm}} \) were similar. The consistency in responses between the different mixing conditions further supports the hypothesis of anoxic zones within the granules.
conditions implied that diffusional limitations were not impacting on the anoxic process rates. The lack of apparent diffusional limitations under these conditions suggested that the rates of anammox consumption were being limited by some other factors such as growth processes; therefore, diffusion was less important.

As DO concentration increased, the NH\textsubscript{4}\textsuperscript{+} conversion rates became more negative and subsequently plateaued at elevated DO values (Figure 3). The highest NH\textsubscript{4}\textsuperscript{+} consumption rates occurred when the DO concentration was the highest as would be expected as the oxygen availability to AOB became non-limiting at high DO values. By contrast, the NO\textsubscript{2} net conversion rates increased and then plateaued as DO increased in the aerobic tests (Figure 3). The results indicate that when the DO concentration was less than or equal to 0.78 mg O\textsubscript{2}/L at G\textsubscript{75 rpm} or 0.46 mg O\textsubscript{2}/L at G\textsubscript{150 rpm}, NO\textsubscript{2} was consumed with the rate of consumption greater than the rate of production, and at higher DO concentrations, NO\textsubscript{2} was produced with the rate of consumption less than the rate of production. Although the trends in net NO\textsubscript{2} conversion rates were similar at G\textsubscript{75 rpm} and G\textsubscript{150 rpm}, the DO concentrations at which the net NO\textsubscript{2} conversion rate equaled to zero were different. At G\textsubscript{75 rpm}, the DO concentration that the net NO\textsubscript{2} conversion rate equaled to zero was between 0.78 and 1.2 mg O\textsubscript{2}/L; whereas at G\textsubscript{150 rpm}, this DO concentration was between 0.46 and 0.76 mg O\textsubscript{2}/L. The different trends in this response as a function of mixing supported the need to further investigate the impact of DO concentration on anammox bacteria by evaluating the observed DO half-velocity constants in the experiments.

The net NO\textsubscript{3}\textsuperscript{−} conversion rates were relatively small relative to the other N species, were always positive, and decreased slightly as DO increased. The decrease of NO\textsubscript{3}\textsuperscript{−} conversion rates was most apparent when the DO concentration was greater than 4.0 mg O\textsubscript{2}/L as most NH\textsubscript{4}\textsuperscript{+} was oxidized to NO\textsubscript{2}. The decrease in NO\textsubscript{3}\textsuperscript{−} conversion rates as DO increased confirmed the low activity of NOB in the system. When DO was lower than 1.0 mg O\textsubscript{2}/L, some NO\textsubscript{3} was produced and this was attributed to anammox bacteria; when DO was higher than 4.0 mg O\textsubscript{2}/L, anammox bacteria stopped producing NO\textsubscript{3}.

The results obtained from the activity testing provided information on the net processes that were active in the tests. However, it was not possible to directly estimate half-velocity coefficients from the data. A model (Ni et al. 2014) that described the active bacterial groups was configured to reflect the batch tests. The model calculates rates of growth and substrate consumption on the basis of bulk liquid substrate concentrations, and the effect of diffusional resistances (external and internal) is embedded in the estimated half-velocity coefficients (extant). The details of the model implementation are described in Supplementary Materials. Default values were assumed for all model parameters (Ni et al. 2014) with the exception of the oxygen half-velocity coefficients for the AOB and anammox species that were estimated by separate multiple response regressions of the data from the two mixing conditions.

The quality of the model fit was assessed by comparing the predicted conversion rates versus the observed rates (Figure 4). Based on the close fit of the data points relative to the perfect fit line and the random distribution of the residuals, it was concluded that the calibrated model successfully described the studied system. Furthermore, the good fit of the model predictions to the observed data for all three nitrogen species over a range of growth conditions indicated that the observed removal rates of the species, relative to each other, were consistent with the theoretical stoichiometric values that were incorporated in the model. The best-fit K\textsubscript{AOB} values were estimated to be 0.54 ± 0.56 and 0.68 ± 0.34 mg O\textsubscript{2}/L for the G\textsubscript{75 rpm} and G\textsubscript{150 rpm} scenarios, respectively, and were found to be statistically similar (p > 0.05). The values were consistent with the range of values that have been reported in the literature and which vary from 0.18 to 1.16 mg O\textsubscript{2}/L (Arnaldos et al. 2015; Ma et al. 2016). The best-fit K\textsubscript{anammox} values were estimated to be 0.55 ± 0.40 and 0.15 ± 0.09 mg O\textsubscript{2}/L for the G\textsubscript{75 rpm} and G\textsubscript{150 rpm} scenarios, respectively, and the former value was determined to be statistically larger than the latter (p = 5.9 × 10\textsuperscript{−10}). Both values were found to be higher than the literature value of 0.01 mg O\textsubscript{2}/L (Vangsgaard et al. 2015; Ni et al. 2014; Corbalá-Robles et al. 2016).

The model employed in this study uses the DO concentration in the bulk liquid to describe the exposure of bacteria to DO. It is believed that this was the primary reason that the estimated K\textsubscript{anammox} values were higher than the literature value, while the K\textsubscript{AOB} values were similar to the literature at both mixing intensities. The literature values
of $K_{AOB}^{O2}$ and $K_{anammox}^{O2}$ were based on bacteria in flocculant systems with minimal mass transfer limitations (Arnaldos et al. 2015; Picioreanu Pérez & van Loosdrecht 2016; Wu et al. 2017). For a reactor with granules composed of different groups of bacteria, the DO concentration decreases from the bulk liquid to the core of a granule (IWA 2006). Therefore, using the DO concentration values in the bulk liquid resulted in the estimated $K_{anammox}^{O2}$ values being larger than the literature value, because the estimated $K_{anammox}^{O2}$ incorporated the effect of all the resistance to DO penetration through the layers surrounding the anammox bacteria core. The similarity in the $K_{AOB}^{O2}$ values in the current study to those in the literature and the lack of the effect of mixing intensities could be attributed to the close proximity of the AOB to the surface of the granules and the absence of a significant mass transfer resistance.

The estimated $K_{AOB}^{O2}$ and $K_{anammox}^{O2}$ values give some insights into the functionality of the different bacterial communities and their abilities to consume substrates in the PN/A process. The TIN removal efficiencies observed in this study indicated that the performance was improved at the $G_{75}$ rpm mixing intensity as compared to that experienced at $G_{150}$ rpm. The results from the batch tests demonstrated that the $K_{anammox}^{O2}$ increased as the mixing speed decreased in Phase 2. Thus, the anammox bacteria experienced less DO inhibition at $G_{75}$ rpm as compared to $G_{150}$ rpm; thereby, the TIN removal efficiency was higher at $G_{75}$ rpm. The results of this study provide process engineers with quantitative information that can be employed to establish mixing conditions for granular PN/A processes that could increase TIN removal performance. Furthermore, the $K_{AOB}^{O2}$ and $K_{anammox}^{O2}$ values developed in this study can be employed to improve models of PN/A processes that quantitatively reflect the impact of mixing conditions on biological process rates.

CONCLUSIONS

In this study, the effects of mixing intensity on a PN/A process were characterized. The steady-state operation was achieved after 83 days of operation at $15 \text{s}^{-1}$ with an average total nitrogen removal of 62%, while after 22 days of operation at $5.5 \text{s}^{-1}$ with an average of total nitrogen removal of 84%. Activity test results showed that as DO increased at both $G$ values, the rates of ammonium consumption increased and then plateaued; the rate of nitrite production increased and then plateaued; and the rate of nitrate
production had no apparent change. The rates of ammonium and nitrite changes plateaued at higher DO values for $G$ values of 5.3 s$^{-1}$ when compared to 15 s$^{-1}$. A bioprocess model was used to estimate the values of $K_{O_2}^{AOB}$ and $K_{O_2}^{anammox}$ from the activity test results. The estimated DO half-velocity constants for AOB were 0.54 mg O$_2$/L at 5.3 s$^{-1}$ to 0.68 mg O$_2$/L at 15 s$^{-1}$ and were not statistically different. The estimated DO half-velocity constants for anammox bacteria were determined to be 0.55 mg O$_2$/L at different.

The estimated DO half-velocity constants for anammox bacteria growth using the DO concentration in the insights that can be employed to simulate AOB and anammox bacteria growth using the DO concentration in the bulk liquid.

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**SUPPLEMENTARY MATERIAL**

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