TIME-RESOLVED EMISSION FROM BRIGHT HOT PIXELS OF AN ACTIVE REGION OBSERVED IN THE EUV BAND WITH SDO/AIA AND MULTI-STRANDED LOOP MODELING

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Received 2015 June 22; accepted 2015 October 22; published 2015 December 23

ABSTRACT

Evidence of small amounts of very hot plasma has been found in active regions and might be an indication of impulsive heating released at spatial scales smaller than the cross-section of a single loop. We investigate the heating and substructure of coronal loops in the core of one such active region by analyzing the light curves in the smallest resolution elements of solar observations in two EUV channels (94 and 335 Å) from the Atmospheric Imaging Assembly on board the Solar Dynamics Observatory. We model the evolution of a bundle of strands heated by a storm of nanoflares by means of a hydrodynamic 0D loop model (EBTEL). The light curves obtained from a random combination of those of single strands are compared to the observed light curves either in a single pixel or in a row of pixels, simultaneously in the two channels, and using two independent methods: an artificial intelligent system (Probabilistic Neural Network) and a simple cross-correlation technique. We explore the space of the parameters to constrain the distribution of the heat pulses, their duration, their spatial size, and, as a feedback on the data, their signatures on the light curves. From both methods the best agreement is obtained for a relatively large population of events (1000) with a short duration (less than 1 minute) and a relatively shallow distribution (power law with index 1.5) in a limited energy range (1.5 decades). The feedback on the data indicates that bumps in the light curves, especially in the 94 Å channel, are signatures of a heating excess that occurred a few minutes before.

Key words: Sun: activity – Sun: corona – Sun: UV radiation

1. INTRODUCTION

The bright curved magnetic flux tubes called coronal loops are the building blocks of the confined solar corona. According to one popular scenario, coronal loops are mainly heated by short and intense energy pulses, called nanoflares (Parker 1988; Cargill 1994; Reale 2014). These pulses might heat the plasma temporarily to temperatures well above the average coronal temperature, and therefore, this scenario is supported by the evidence for small amounts of ultra-hot (>5 MK) plasma in non-flaring active regions (McTiernan 2009; Reale et al. 2009a, 2009b; Testa et al. 2011; Miceli et al. 2012; Testa & Reale 2012; Brosius et al. 2014; Petralia et al. 2014; Caspi et al. 2015).

According to several recent works (Klimchuk et al. 2008; Cargill et al. 2012; Viaggi & Klimchuk 2012), heat pulses are released at spatial scales smaller than the typical resolved loop cross-section. A single loop must then be sub-structured into a bundle of thin strands where the plasma can move and transport energy along the magnetic field lines independently of the others, under the effect of each localized heat pulse. Since the strands are under-resolved at the moment, the cross-section of the smallest components is under debate (Brooks et al. 2012; Peter et al. 2013). On the other hand, the very efficient thermal conduction along the magnetic field lines at coronal temperatures also inhibits the measurement of the duration of the individual heat pulse.

This work extends the analysis of an active region that has shown evidence of small amounts of very hot plasma (>5 MK) in most of the region core and out of proper flares (Reale et al. 2009a, 2011; Testa & Reale 2012). This area is appropriate to search for signatures of small scale heat pulses.

We investigate the emission variability at the smallest possible scale and look for signatures of heating and possibly elementary heating events. We model the extreme ultraviolet emission observed by the Solar Dynamic Observatory (SDO) from the active region core using a hydrodynamic model of bundles of strands heated impulsively. In the active region core we extract the light curves of both a sample single pixel and a row of neighboring pixels in different channel bands. We generate model light curves by summing over random events with different energy and we compare them to observed ones using two independent methods: an artificial intelligence system based on a probabilistic neural network (PNN) and a simple cross-correlation technique. The simultaneous comparison of the light curves in different channels allows us to address the multi-temperature structure of the loop, which is a key point when we consider such a structured heating.

2. OBSERVATIONS

We study an active region with evidence of small quantities of very hot plasma that may be a signature of short and intense heat pulses (Reale et al. 2011). The data and their basic processing have been already described in Reale et al. (2011). We select some specific pixels in the core of this active region. In particular, we initially chose the observations in three EUV channels, namely 94 Å, 171 Å, and 335 Å, that are most sensitive to the emission of plasma in a broad range of temperatures, i.e., at 6 MK, 1 MK, and 3 MK, respectively. The response function in the 94 Å channel is double peaked, with a cooler peak below 1MK (Boerner et al. 2012, 2014; Testa et al. 2012). However, in active region cores the hotter peak is generally dominant (e.g., Testa & Reale 2012).
For our study we need the highest possible space and time resolution to try to capture the small temporal and spatial scales expected for nanoflare heating. Therefore, we consider the smallest scale pixel region, i.e., single pixels, and the full time resolution. Figure 1 shows the active region core in the three AIA channels and the location of the pixels where we have extracted light curves. We have not chosen the 171 Å channel for further analysis because it is severely affected by underlying moss emission, i.e., emission coming from the bright footpoints of hot loops (Peres et al. 1994; Fletcher & de Pontieu 1999). By definition, this emission is not included in our modeling, which comprises only the coronal part of the loops. Since this emission is out of the scope of our work, from now on we will address only the comparison with the 94 and 335 Å channels, which instead are sensitive to the body of the coronal loops. We have ascertained that the low temperature contribution to the 94 Å channel is negligible (by rescaling the emission in the 171 Å channel, e.g., Reale et al. 2011).

We consider 246 and 228 successive images in the two respective channels, corresponding to timeseries of a total...
duration of \( \sim 1 \) hr, i.e., much longer than typical loop plasma cooling times (Reale 2014). The exposure time is 2.9 s in both channels. We carefully aligned images between the two different channels via cross correlation using the align_cube_correl procedure in SSW. The time distance between the images is typically 12 s, but there are some gaps up to \( \sim 1 \) minute. We select a single pixel in the bright and filamented core observed in the 94 Å channel, where there is evidence of very hot plasma (Reale et al. 2011). It is one where the light curve does not show prominent single-time spikes, which typically affect other pixels. We have also tried to improve the signal-to-noise ratio. Our choice has been to sum the emission in a few nearby pixels. The orientation of the observation frame versus the active region shows that many structures are practically aligned in a left to right direction. Actually, we have identified a few rows of pixels where the emission shows coherent time behavior, i.e., they probably intercept the same loop strands where the confined plasma evolves coherently. We select a row of nine pixels that includes the single pixel. Figure 2 shows the light curves for the single pixel and for the row of nine pixels. To better show the trends and features of the single pixel emission, we also show the light curves smoothed with a boxcar of eight data points. The single pixel allows for the maximum possible sensitivity to emission variations, but is affected by significant noise from limited photon statistics. The row of pixels reduces the photon noise but also the sensitivity to variations. The light curves show different amplitudes of fluctuations in the two channels. The evolution in the 335 Å channel is rather smooth, with an overall variation range of \( \sim 30\% \). In the 94 Å channel we see larger fluctuations and even a localized peak \( \sim 50\% \) above the average with a duration of \( \sim 5 \) minutes. The bump shows equal rise and decay times. We find similar trends and features and similar analysis results for other pixels.

From the observation, we estimate that the loops inside the active region core have a length of \( \approx 5 \times 10^9 \) cm and we will assume this as our reference loop length from now on.

3. THE ANALYSIS

3.1. The Loop Model

Our aim is to analyze the time variation of the loop emission. Under the reasonable assumption that the plasma evolution does not change much from one position to the other inside a single strand that composes the loop, we focus on the description of the strand population, of the parameters of the related storm of nanoflares, and of how they combine to produce the total observed emission. In this scenario, the coronal average quantities in each strand provide enough information to describe the strand properties, but we need a good description of their time evolution.
To this purpose, we use EBTEL (Enthalpy Based Thermal Evolution of Loops), a zero dimensional time-dependent hydrodynamic model (Klimchuk et al. 2008; Cargill et al. 2012). The model has no spatial resolution and describes the evolution of the average physical properties of the plasma confined in a single coronal flux tube. The model assumes that the loop is symmetric with respect to the apex, and therefore describes half of it. A physical key concept in the model is the enthalpy, which has the main role in transferring the energy budget into and out of the corona. The enthalpy will certainly not produce or eliminate energy. Variations in the heating rate will affect the transfer of mass between the chromosphere and corona. Any changes in the heating rate will cause an increase or decrease in the heat flux and any excess or deficit in downward heat flux related to the transition region radiation loss will consequently derive an upflow enthalpy flux or will be compensated by a downward enthalpy flow, respectively. The energy equation is

$$\frac{\partial E}{\partial t} = \frac{\partial(Ev)}{\partial s} - \frac{\partial(Pv)}{\partial s} - \frac{\partial F}{\partial s} + \bar{Q} - n^2 \Lambda(T) + \rho g_{\parallel}$$  \hspace{1cm} (1)

in which

$$E = \frac{3}{2}P + \frac{1}{2}m^2.$$  \hspace{1cm} (2)

$E$ is the combination of thermal energy and kinetic energy, $P$ is pressure, $v$ is the bulk velocity, $F$ is the heat flux, $\bar{Q}$ is the volumetric heating rate, $n$ is the electron density, $\Lambda$ is the radiation loss function, and $g_{\parallel}$ is the gravity component which is along the magnetic field. We assume classical conductivity, but we have ascertained that saturated conductivity does not change the results (and in particular the light curves; see Section 4) significantly on the relatively long timescales of our modeling. The evolution for density and pressure can be described fully versus the coronal parameters, as we integrate the energy equation over the coronal part of the loop once and separately over the transition part.

$$\frac{1}{\gamma - 1} \frac{d\bar{P}}{dt} = \bar{Q} - \frac{1}{L} (R_c + R_a)$$  \hspace{1cm} (3)

$$\frac{1}{\gamma - 1} \frac{d\bar{n}}{dt} = \frac{n_0 v_0}{L} = -\frac{\gamma - 1}{2KT_eL}\left(F_0 + R_a\right)$$  \hspace{1cm} (4)

where $\bar{P}$ and $\bar{n}$ are the averages of pressure and density, $R_c$ and $R_a$ are the radiation losses in the corona and transition region, respectively, $F$ is the heat flux, $v$ is the bulk velocity, and 0 indexes describe the values in the base of the corona. This set will be completed if we insert an equation of state.

$$\frac{1}{\bar{T}} \frac{d\bar{T}}{dt} = \frac{1}{\bar{P}} \frac{d\bar{P}}{dt} - \frac{1}{\bar{n}} \frac{d\bar{n}}{dt}.$$  \hspace{1cm} (5)

We use EBTEL to model the evolution of the plasma confined in single loop strands under the effect of short heat pulses. Figure 3 shows the evolution of average coronal temperature and density inside a single strand subject to impulsive heating. The strand is initially cool and tenuous, with a temperature of 0.24 MK and a density of $\sim 10^{6} \text{cm}^{-3}$. A very small amount of heating ($10^{18} \text{erg cm}^{-3} \text{s}^{-1}$) is constantly provided to keep the strand in equilibrium. In addition to this, we impose a heat pulse with a triangular time profile having a duration of $\tau = 50 \text{s}$ and an intensity peak of $h = 0.003 \text{erg cm}^{-3} \text{s}^{-1}$. This heating rate corresponds to a temperature of $\sim 2.5 \text{MK}$ at the equilibrium according to the scaling laws of Rosner et al. (1978). The thermodynamic decay time according to Serio et al. (1991) and Reale (2014) is $\tau \approx 800 \text{s}$. We follow the evolution over $10^{4} \text{s}$, i.e., more than 10 decay times in this case.

In Figure 3 the temperature rises abruptly to $\sim 3 \text{MK}$ as a consequence of the intense nanoflare. The strong heat flux drives massive evaporation from the chromosphere to the corona and the strand begins to fill with plasma to a maximum density of $\sim 2 \times 10^{13} \text{cm}^{-3}$. This is much lower than the equilibrium density of $\sim 3 \times 10^{13} \text{cm}^{-3}$ because of the short duration of the heat pulse. The temperature declines as the nanoflare shuts off by the effect of both the radiation and plasma thermal conduction toward the cool chromosphere. The density peaks later (by $\sim 10 \text{minutes}$) than the temperature because the evaporation continues for some time (Reale 2014). The strands finally enter a long phase of draining as the radiation loss—the cooling mechanism—gradually overcomes the thermal conduction (Cargill et al. 2012). The density decay is much slower than the temperature decay.

From the EBTEL results we can derive the emission in the EUV. Figure 3 shows the light curve in the SDO/AIA 94 Å channel. The light curve has a shape in between the evolution of the temperature and of the density, because the emission is a function of both of them. So, the peak of the emission occurs $\sim 5 \text{minutes}$ later than that of the temperature. This is the light curve of a single strand. When we look at the light curve of a pixel, we are summing the light curves of many strands that are intercepted along the line of sight in that pixel.

A single pixel may contain tens to several hundreds of strands, each heated impulsively. We assume that the distribution of the heat pulses is described by a power law (e.g., Hudson 1991):

$$dN = E^{-\alpha}dE$$  \hspace{1cm} (6)

where $dN$ is the number of events per energy interval ($E$, $E + dE$) and $\alpha$ is the power law index. Each strand is ignited independently of the others, and therefore at random times and at random intensities, according to the power law frequency distribution. Since we are unable to constrain the times and intensities, our approach is to generate a large number of different realizations of the same light curve that consists of overlapping light curves of a given number of strands. Each light curve is related to a random pulse extracted from the power law distribution and has a random start time. We generate groups of realizations, one for a given power law index, pulse duration, and number of strands.

As mentioned in Section 2, the total loop length is fixed to $5 \times 10^{6} \text{cm}$. We chose two possible values of the power law index, i.e., $\alpha = 1.5$ and $\alpha = 2.5$. We chose either of two possible pulse durations, i.e., a short ($\tau = 50 \text{s}$) one and a long ($\tau = 500 \text{s}$) one, with respect to typical plasma cooling times. The other key parameter is the number of strands that are heated along the line of sight, and in particular we consider three possible values, $N = 10$, 100, and 1000. We assume that each strand is heated only once during our total time lapse. In this view, the number of strands is also the number of heat pulses. There is discussion about the frequency of the heat pulses inside a single strand and whether the repetition time is large (low frequency) or small (high frequency) with respect to the typical cooling times (Klimchuk 2015). Our scenario is
basically low frequency. However, we address only the high
temperature emission, and similar results might be obtained
with more frequent pulses, with a delay not much longer than
1000 s (see Figure 3(c)). This might be in agreement with
recent constraints (e.g., Cargill 2014; Cargill et al. 2015).

The observed light curves fluctuate around a steady value.
When we generate events at random times and overlap them,
we have to wait until a steady state is reached. We found that a
safe time lapse to reach steady state is half an hour (1800 s).
Therefore, we assume that all the events occur at random times
within the total observation time, i.e., 3576 s plus half an hour,
and therefore in a time range \(0 < t < 5376\) s. When we
compare our results with the observations we will consider only
the final 3576 s, in which we are sure that the simulated
emission is as steady as the observed one. In the following all
the model light curves will start from \(t = 1800\) s, which will be
assumed as the reference time.

We tune the range and height of the power law distributions
so as to produce a bundle of strands that has the average
temperature of the observed active region loops, i.e., about
3 MK. Figure 4 shows the energy rate distributions of the
pulses obtained for different numbers of strands and for the
shorter pulse durations. Instead of producing one model for
each energy rate, i.e., for each realization, we preferred to
generate a grid of EBTEL models, choosing the parameters so
as to reasonably span all possible loop conditions in the energy
range. We then use a binary search to find the closest value of
each energy from the original power law distribution to the one
in the grid.

For each of the 12 combinations of \(\alpha, \tau,\) and \(N,\) a package of
10,000 pairs of light curves (two for each realization) is
produced. We compare each pair of light curves to the observed
ones and choose the best matching ones with the methods
described in the following.

### 3.2. Probabilistic Neural Network

We employed PNN (probability neural network), a kind of
artificial network which is suitable in classifying and identify-
ing the samples. Recently it has been successfully applied in
every field of science as a classifier machine. The main and first
step in performing a comparison with this tool is to train the
network by training samples. During the training session the
network will learn the possible determined classes. The
architecture of a PNN that shows a complete training session
is shown in Figure 5.
When an input vector is fed to the network, the first layer computes the distance from the input vector to the training samples. This produces a vector that indicates how close the input is to the training samples. The second layer sums the contribution for each class of inputs and produces its net output as a vector of probabilities. Finally, the "compete" transfer function on the output of the second layer picks the maximum of these probabilities and produces 1 (positive identification) for that class and 0 (negative identification) for non-targeted classes. In this way the network will match each tested sample to its own class of trained samples (Bazarghan et al. 2008; Tajfrouze & Safari 2012).

The PNN is a supervised algorithm that needs to be trained before being used for classification. Therefore, the greater the number of training samples we provide to feed the network, the more accurate the output of PNN will be. Its performance is based on estimating the probability density function from sample patterns, which implicitly consists of calculating the distances between an input vector with the other training samples. So, it seems to work just like a nearest neighbor classifier (Montana 1992, p. 1110) while comparing to other kinds of classification methods. For this reason, it can better deal with irrelevant features.
3.3. Cross Correlation

The other method we use is cross correlation, which is simply a way to measure how similar the signals are. This kind of approach has been recently applied to the analysis of coronal observations (Viall & Klimchuk 2013). Two input vectors \( x \) and \( y \) may be cross-correlated as a function of time lag \( L \) as:

\[
\text{corr}_{x,y} = \frac{\sum_{i=0}^{M-|L|-L}(x_{i+L} - \bar{x})(y_{i} - \bar{y})}{\sqrt{\sum_{k=0}^{M-1}(x_k - \bar{x})^2 \sum_{k=0}^{M-1}(y_k - \bar{y})^2}} \quad \text{for } L < 0
\]

\[
\text{corr}_{x,y} = \frac{\sum_{i=0}^{M-|L|-L}(x_{i} - \bar{x})(y_{i+L} - \bar{y})}{\sqrt{\sum_{k=0}^{M-1}(x_k - \bar{x})^2 \sum_{k=0}^{M-1}(y_k - \bar{y})^2}} \quad \text{for } L \geq 0
\]

where \( \bar{x} \) and \( \bar{y} \) are the averages of the vectors \( x = (x_0, x_1, \ldots, x_{M-1}) \) and \( y = (y_0, y_1, \ldots, y_{M-1}) \), respectively (\( M \) is the number of data points).

The function \( \text{corr}_{x,y} \) within the IDL software enables us to find the correlation values between two selected samples at any given time lag. The highest similarity between two samples will be indicated by the maximum cross-correlation value.

4. RESULTS

The next step is to compare these light curves to the observed ones and to find the best match for each combination independently with both the comparison methods. Our key point is to find the realization that best matches the light curves in both channels at the same time.

With the PNN method we are not able to compare pairs of light curves simultaneously, but only one model light curve with one observed light curve at a time. Since we want to simultaneously match light curves in two different channels, our solution has been to join each light curve in one channel to the corresponding light curve in the other channel. So, we first normalize each light curve to its maximum value, and then we stitch the end point of one to the first point of the other. This is done for both the simulated and observed light curves.

Afterward, we trained the network with the simulated light curves as training samples. The observed light curves are then fed to the network as the test samples for classification with respect to the training samples. The process of classifying the data is done for the light curve of the single and the row of pixels separately.

The output of the network finds the best choice among the available set of simulated patterns that best resemble the data and labels it with its own corresponding key parameters. In Figure 6, for each of the 12 sets of parameters, we show the light curves of the realization that best match the observed ones according to the PNN method. For a better visual comparison, we have applied normalization, smoothing, and shifting procedures, but we remark that the PNN compares the realizations with the original light curves (after a normalization only).

In general, the PNN is unable to find simulated patterns that perfectly match the observed ones, not even in one channel. The PNN chooses the best solution as the one that shows the best match of the overall general patterns. As mentioned above, we let the method find the best solution for each set of parameters. The best absolute solution remains to be found. We might rank the best solution on its overall ability to reproduce the details of the observed features, and in particular the amplitude, shape, and timescale of the observed bumps in both channels. From a visual inspection of Figure 6 we realize that the best solutions are not equivalent. Those with a long pulse duration, with a small number of strands, and with a steep distribution all show features that are too broad, which do not fit the observed features on the smallest timescales, especially in the 94 Å channel. The solutions with a steeper distribution (\( \alpha = 2.5 \)) are also in general unable to reproduce the variability on short timescales. A small number of strands determines too strong bumps in the 335 Å channel. The best absolute solutions appear to be those with a flatter energy distribution and shorter pulse duration. Among these, the one with the largest number of strands yields the lowest total root mean square deviation (RMSD) from the observed light curves, defined as

\[
\text{RMSD} = \sqrt{\frac{1}{M} \sum_{i=1}^{M} (R_i - \bar{O}_i)^2}
\]

where \( R_i \) are the model intensities normalized to their average (for each channel) and \( \bar{O}_i \) are the observed intensities normalized to their average. So, eventually, the best set of parameters found with PNN is \([\alpha = 1.5, \tau = 500, N = 1000]\) (thick black lines in Figure 6), for which we obtain RMSD = 0.21.

Two points here are worthy of being pointed out. One is the fact that the network is not sensitive to denoising or smoothing (Tajfrouze & Safari 2012). Another point is that the output of the network does not change even when we reverse the order of stitching the light curves. This means that the network is robust in its performing.

We make an alternative comparison using the simple cross-correlation technique described in Section 3.3. With this method we can compare the simulated and observed light curves of both channels simultaneously without joining them. In a given channel, each model light curve is time-shifted and cross-correlated with the observed one (either the single pixel or the pixel row), and the cross-correlation value is computed. As we did for PNN, we do this for each set of parameters. The best match is given by the realization that provides the highest sum of cross-correlation values found for the two channels and the same time lag. The best matching realizations for each set of parameters found with cross-correlation are shown in Figure 7 (see Figure 6 for comparison).

The best absolute matching (and the highest cross-correlation value) is obtained by the same set of parameters as that found with the PNN method, i.e., \( \alpha = 1.5, \tau = 50, N = 1000 \), although with a different realization (thick black lines in Figure 7). However, for this realization we obtain RMSD = 0.24, which is slightly higher than that obtained with the PNN method.

We obtain very similar results when we compare the model realizations with the observed light curves extracted from the row of pixels, i.e., the same best set of parameters with both PNN and cross correlation. In the following, we will consider the best solution found for the single pixel and with the PNN method as the best absolute one.

It is interesting to make considerations about the absolute intensity values. We first compare the ratio of the mean observed intensities with those of the best realization. We obtain \( (I_{335}/I_{94})_{\text{obs}} \approx 5.1 \) versus \( (I_{335}/I_{94})_{\text{mod}} \approx 5.5 \). The
agreement is remarkable, with the percent difference (∼7%) being less than the average fluctuations of the 94 Å light curve (∼15%). The slightly higher emission observed in the 335 Å channel might be simply due to some diffuse emission along the line of sight. Figure 8 shows the best matching model alone. In this figure we go back to the original intensities with no normalization. To compare the model results to the observations we have to make an assumption about the cross-section of the strands. We find that we need a cross-section of 0.56 and 0.52 pixels in the 94 Å and 335 Å channels, respectively, to match the best model to the observed light curves. Under the assumption of 1000 equal and independent strands, this is equivalent when each strand has a thickness of ∼10 km. This becomes a lower limit if the strands are not entirely independent, i.e., if the same strand is heated more times during our time lapse (see Section 3.1). We should also keep in mind that we have a logarithmic spacing in our sampling of the number of strands, and therefore this value of the thickness should be taken with care.

5. DISCUSSION AND CONCLUSIONS

In this work we analyze the time evolution of the EUV emission in the core of an active region, which shows evidence for a very hot \( (T > 5 \text{ MK}) \) plasma component (Reale et al. 2011). This hot component might be a signature of the occurrence of rapid but intense heating releases, which bring the plasma to such high temperatures for short times. In that active region we consider the light curves at the maximum time resolution in three SDO/AIA channels picked up either in a single pixel or in a row of pixels where the emission evolves coherently.

We try to match the observed light curves with the emission derived from specific loop modeling. The simultaneous presence of very hot plasma and steady emission indicates that we might have storms of events with a broad range of energy distributions. In light of this evidence, our choice has been to describe the evolution in a scenario of loops made by bundles of independent strands each heated for a time shorter than the typical plasma cooling times (e.g., Guarrasi...
We assume that each strand is tenuous and cool at the beginning and is heated only once, at a random time, by a heat pulse of random intensity. It is then left free to decay. This is equivalent to fewer strands heated repeatedly but not at a high frequency, i.e., after time intervals longer than the cooling and draining times (Warren et al. 2010; Klimchuk 2015, see also Section 3.1).

Since we address the time evolution only, and no spatial issues, we preferred to consider the very efficient approach of 0D loop modeling, which describes the evolution of the average quantities of the coronal plasma contained in a loop magnetic flux tube. The output of the model is the evolution of the average density and temperature, which we use to derive the light curves in relevant channels to be compared with the observed ones. An important issue is the choice of the free parameters. We assume that all strands have the same length, which is constrained from the observation. We observe mostly straight bright structures in the core of the active region deep in the disk, so we assume semicircular strands that stand vertically from the surface. The other important parameters are the intensity of the heat pulses, their duration, and the number of strands. In the framework of randomly occurring events, we assume that the heat pulses are distributed as power laws.

Figure 7. As in Figure 6, according to the cross-correlation method.

Figure 8. Model light curves (black lines) in the AIA 94 Å channel (upper panel) and 335 Å channel (lower panel) for the case \( \alpha = 1.5, \tau = 50, \) and \( N = 1000 \), best matching the observed ones (red lines) found with the PNN method. This is the best absolute match. The model intensities are scaled to match the average observed intensities by assuming a total cross-section area of 0.56 and 0.52 pixels, respectively.
assume two possible values of the power law index, i.e., a shallower ($\alpha = 1.5$) and a steeper ($\alpha = 2.5$) one. We then normalize the intensity and range of the distribution to find an average heating rate that is able to produce a loop plasma at 3 MK on average, according to the loop scaling laws. We set two possible durations of the heat pulses, a short (50 s) and a long (500 s) one. The number of strands changes logarithmically, from a few ($10^{1}$) to a relatively large number ($10^{3}$). For each of the two pulse distributions with different $\alpha$ and of the two pulse durations, we generate a grid of 0D models. For each model we derive the light curves in the AIA 94 and 335 Å channels. The next step has been to choose the number of strands and to combine randomly the corresponding number of light curves in a channel according to one of the pulse distributions and for one pulse duration. So we randomly pick up an intensity from the intensity distribution and a random start time of the pulse, uniformly distributed in a time range of 10,000 s. For each set of parameters we derive 10,000 different realizations, i.e., random combinations of light curves in the 94 and 335 Å channels. Each pair of light curves has been compared to the pair of observed ones. The comparison has been made independently with two different methods, one based on artificial intelligence, the other on a simple cross correlation. We do not address a perfect match of the simulated and observed light curves, which would require much larger sets of realizations. We let the methods find the best realizations for each set of parameters. Then, we compare these best cases and pick up the one that is able to reproduce patterns globally similar to the observed ones, and in particular variations with similar amplitude and timescales and similar shapes of the local emission bumps or dips.

The parameter set of the realization that best matches qualitatively and quantitatively the observed light curves is a shallow power law index ($\alpha = 1.5$), a short pulse duration (50 s), and relatively large number of strands ($10^{3}$). This realization has been singled out with the PNN method, minimizes the deviations from the observational data, is able to reproduce many features of the observed light curves, and delivers a ratio of the intensities that is consistent with the observed ones. Realizations with the same set of parameters best match the light curves both of the single pixel and of those averaged over a row of a few pixels.

The distribution of events is able to describe the presence of both many weak and few strong events, which explains both the rather smooth light curves and the presence of a small amount of hot plasma at the same time. The relatively small

\textbf{Figure 9.} Time evolution of (a) temperature, (b) density, and (c) heat pulses of all the randomly heated strands that overlap to build the model light curve in Figure 8. The red lines are the average values. Time has been shifted by 1800 s.
duration of the heating release, of the order of 1 minute, is in agreement with recent finding from observations and modeling (Testa et al. 2013, 2014). A relatively high number of heated strands is preferred, and is able to reproduce well the rather steady emission. We find that the intensities from this combination of parameters are compatible with strands $\sim 10$ km
thick or more, to be compared with recent measurements (~100 km) from high resolution observations (Brooks et al. 2013).

The simulated light curves that best match the observed ones show that the emission fluctuates more in the 94 Å channel, and it is smoother in the 335 Å channel, which is more sensitive to cooler plasma. However, we can see a large scale similarity in the global trends. Figure 9 shows the evolution of the plasma and heating event properties for all the modeled strands. In the temperature plot, among the multitude of lower temperature events, we clearly distinguish a smaller number of events that bring the temperature above 10 MK for short times. They are consistent with the detection of a small and filamented amount of very hot plasma in this region (Reale et al. 2011). It is interesting to search for signatures of physical processes in the light curves. Figure 10 zooms in on a 1000 s time range of Figure 9 and shows the temperature events, the distribution of heat pulses, and the evolution of the average event heating rate, with a 50 s time binning. While we do not see any obvious correspondence between the light curves and the first two quantities, we clearly see a correlation of the event heating rate with the trends observed in the light curves. In particular, we see a train of heat bumps that anticipates a train of emission bumps by ~200 s in the 94 Å channel. This time lag is of the same order as the delay between the temperature peak and the emission peak for a single strand shown in Figures 3(a) and (c) (see also Section 3.1), ultimately due to the more gradual evolution of the density. We might therefore infer that strong fluctuations in the 94 Å channel probably mark a previous increment of heating episodes with a delay of a few minutes. This signature is also present in the 335 Å channel, but is much less significant.

Overall, the analysis presented here shows results that are consistent with previous works. The short and infrequent heat pulses are largely consistent with the presence of cooling plasma for most of the time, which was detected in Hinode/XRT observations (Terzo et al. 2011) and in SDO/AIA observations (Viall & Kilchuk 2012). In the former work, a good match with observations is obtained with Monte Carlo simulations, including most energetic random pulses at an average time distance of 360 s from each other. From Figure 10 we can count ~30 high pulses (0.4 erg cm$^{-3}$ s$^{-1}$, with a comparable peak temperature and duration with those in Terzo et al. 2011) in ~1200 s, corresponding to an average time distance of ~150 s. This higher frequency is not included in Terzo et al. (2011) and might be consistent for the core of an intense active region. The model also involves the presence of very hot plasma as detected in the same region analyzed here in SDO/AIA observations (Reale et al. 2011). Our analysis obtains additional information about the number, distribution, and intensity of the heating events and about the fine loop structuring, and figures out a possible signature of the heating directly detectable in the light curves.

This work also improves on the previous analysis with artificial intelligence methods (Tajfrouze & Safari 2012), because we specifically use a loop model as the basic model, we address simultaneously matching the light curves in two different channels, and we cross-check with a different comparison method, namely cross correlation.

A further improvement on our analysis could be the attempt to also include some spatial information, i.e., the coherence of the signals in the same loop structures. This requires using more detailed loop models that describe the confined plasma with spatial resolution.

We thank the referee for very constructive comments, and Dr. T. Di Salvo for suggestions. E.T., F.R., and A.P. acknowledge support from Italian Ministero dell’Università e Ricerca. P.T. was supported by contract SP02H1701R from Lockheed-Martin to the Smithsonian Astrophysical Observatory, and by NASA grant NNX15AF50G. SDO data was supplied courtesy of the SDO/AIA consortia. SDO is the first mission to be launched for NASA’s Living With a Star (LWS) Program.

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