Abstract

Self-instigated isolation is heavily relied on to curb severe acute respiratory syndrome coronavirus 2 (SARS-CoV-2) transmission. Accounting for uncertainty in the latent and prepatent periods, as well as the proportion of infections that remain asymptomatic, the limits of this intervention at different phases of infection resurgence are estimated. We show that by October 2020, SARS-CoV-2 transmission rates in England had already begun exceeding levels that could be interrupted using this intervention alone, lending support to the second national lockdown on 5th November 2020.

A general population lockdown occurred in England on 23rd March 2020 to reduce severe acute respiratory syndrome coronavirus 2 (SARS-CoV-2) transmission. This drastic intervention successfully inhibited disease spread by rapidly depleting the opportunities for transmission events between infected and susceptible people remaining in general circulation [1]. Subsequent to easing out of lockdown from 4th July 2020, infections resurged and England entered its second national lockdown on 5th November 2020. The return of millions of (largely susceptible) people to general circulation underlies the epidemic re-entering an exponential growth phase. However, also culpable in the current public health emergency is the failure of interventions during the period following lockdown’s release.

Contact tracing endeavours in 2020 to reduce SARS-CoV-2 transmission have been ineffective in England and so isolation has been primarily instigated by those responding to symptoms’ development in themselves or their close associations [2]. The mechanism by which this reactive isolation operates is importantly distinct from pre-emptive mass quarantine (lockdown). Symptoms-prompted, reactive isolation only applies to individuals who are infected (cf. the total population), and, more specifically, to those who register symptoms. Hence, infectious individuals who have not yet experienced symptoms, or who will never experience them, are missed.

The mathematical epidemiology of reactive isolation is fairly nascent yet critical in the context of the current epidemic. Here, we generate estimates for reactive isolation thresholds that account for uncertainties in the latent and pre-patent period of infection as well as in the proportion of infected individuals that register and respond appropriately to symptoms.

Mathematical derivation of reactive self-isolation

Beginning with the simplest derivation for physical isolation: the pre-emptive quarantine threshold proportion (Q) is $Q > (1 - (1/R))$ where ‘R’ is the reproduction number [3]. For reactive isolation ($Q^*$), this threshold is inflated to account for the leaked infections occurring because of the delay between becoming infectious and first exhibiting symptoms: $Q^* > (1 - (1/R)) \times \frac{1}{1 - ((p - l)/g)}$. Respectively, $p$ and $l$ are the prepatent and latent periods of infection (in days), and $g$ is the time until recovery (12 days on average [4]). If symptoms typically develop at the same time as an individual becomes infectious, the square-bracket component equals one and the original threshold ($Q$) is regained. A further modification can be made to account for the proportion of infections that never give rise to symptoms (denoted ‘a’): $Q^{**} > (1 - a) \times (1 - (1/R)) \times \frac{1}{1 - ((p - l)/g)}$. For example, if half of infections remained asymptomatic, the proportion of symptomatic infections that need to be isolated to achieve an equivalent impact must be doubled. As with those who never develop symptoms, individuals who fail to respond appropriately to developing symptoms – early indication is that this is not a negligible proportion [5] – will continue to contribute to transmission, so ‘a’ could be considered a composite of these two proportions.

Accounting for uncertainty in parametrisation

The latent and prepatent periods are quite variable for coronavirus disease 2019 (COVID-19) patients. Instead of single-point estimates for these parameters, collated data form a distribution of reported times. The latent period is drawn at random from a Weibull distribution and
then subtracted from the random draw from a second Weibull distribution depicting the range of reported prepatent periods. Figure 1a illustrates these distributions as informed by the clinical and epidemiological literature [6–8]. Also shown is the distribution of times between development of infectiousness and symptom onset as fitted to 10,000 random draws. The distributions of prepatent and latent periods overlap so to avoid the possibility of symptoms developing prior to infectiousness, random draws whereby infectiousness trailed the day of symptoms onset were removed and resampled. In total, 10,000 random draws were then made from this newly derived distribution of the delay between infectiousness and symptoms, and the isolation threshold (Q*) was estimated for a range of R values and a range of asymptomatic proportions (Python code for this analysis is freely available at https://github.com/lwyakob/COVIDquarantine).

**Isolation thresholds accounting for uncertainty**

Figure 1b shows the mean isolation threshold required to control SARS-CoV-2 accounting for the range of estimates for the prepatent and latent periods. The value for R is dynamic, varying according to current intervention effectiveness and population-level susceptibility, so the isolation threshold is shown for a range of plausible R values. The form of the relationship between Q* and R shows an isolation threshold that increases asymptotically with reproduction number. However, allowing for uncertainty in prepatent and latent periods results in a wide 95% prediction interval. The interpretation is that when accounting for both the uncertainty in estimating the population mean, plus the random variation of the individual values, reactive isolation cannot interrupt transmission (at least 95 times out of 100) if R already exceeds a value of ∼1.7 (blue cross in Fig. 1b marks the R value whereby the isolation threshold proportion exceeds unity).

Reactive isolation is further limited when asymptomatic infections comprise a non-negligible proportion (alternatively, when those exhibiting symptoms fail to isolate themselves to some degree). Figure 1c shows the theoretical limits of the proportion of infections that can be asymptomatic and yet SARS-CoV-2 transmission interrupted through isolating symptomatic individuals (using the Q** expression). Superimposed on this trade-off between the reproduction number and the isolation threshold are estimates for R in England as of October 2020 [9, 10], and the 95% confidence and predictive intervals for the proportion of infections that remain asymptomatic as generated by a living systematic review [9]. Respectively, by October, 75% and 85% of these parameter spaces were already beyond the level at which reactive isolation can be sufficient to interrupt transmission (i.e. these regions fall to the right of the hatched arc in Fig. 1c meaning the isolation threshold proportion exceeds unity).

**Limitations and future research**

One limitation of the current analysis is the consideration of transmission and control at the population level rather than stratified by various risk factors. To address this, results were generated for a full range of R values. It is important to note that...
stratification would impact the derivation of $R$ but not the population-level isolation thresholds calculated for a given $R$ value [11]. Another limitation is the implicit assumption that, in the absence of intervention, asymptotically infected individuals contribute to onwards transmission as much as symptomatically infected individuals. It is unclear how questionable this assumption is but clinical studies indicate that asymptomatic and symptomatic individuals have similar viral loads [12]. Should evidence arise of their differential contributions to transmission, the model and code associated with this study can be modified easily to account for this feature.

Even during pre-emptive quarantine (i.e. lockdown) the formulae described here continue to apply to those who remain in general circulation (e.g. essential personnel). Future research should look at how isolation thresholds can be estimated to inform this intervention combination, among others.

Financial support. The author received no financial support for this work.

Conflict of interest. None.

Data availability statement. Data and model code are all available from https://github.com/lwyakob/COVIDquarantine.

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