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To cite this version:

Ivan Latella, Agustín Pérez-Madrid, J Miguel Rubi, Svend-Age Biehs, Philippe Ben-Abdallah. Heat Engine Driven by Photon Tunneling in Many-Body Systems. Physical Review Applied, 2015, 4 (1), pp.011001. 10.1103/PhysRevApplied.4.011001. hal-01335155

HAL Id: hal-01335155
https://hal-iogs.archives-ouvertes.fr/hal-01335155

Submitted on 21 Jun 2016

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Heat Engine Driven by Photon Tunneling in Many-Body Systems

Ivan Latella, Agustín Pérez-Madrid, J. Miguel Rubi, Svend-Åge Biehs, and Philippe Ben-Abdallah

Abstract

Near-field heat engines are devices that convert the evanescent thermal field supported by a primary source into usable mechanical energy. By analyzing the thermodynamic performance of three-body near-field heat engines, we demonstrate that the power they supply can be substantially larger than that of two-body systems, showing their strong potential for energy harvesting. Theoretical limits for energy and entropy fluxes in three-body systems are discussed and compared with their corresponding two-body counterparts. Such considerations confirm that the thermodynamic availability in energy-conversion processes driven by three-body photon tunneling can exceed the thermodynamic availability in two-body systems.

A heat engine may, in general, be conceived as a device that converts part of the heat coming from a hot source of energy into mechanical work throughout an appropriate conversion system [1]. In contactless devices, this heat is transferred to the converter by radiation, only. At long separation distances, the maximum power which can be transmitted is bounded by the blackbody limit [2]. On the contrary, at separation distances smaller than the thermal wavelength, heat can be transferred to the converter also by photon tunneling, so that the flux can become several orders of magnitude larger than in the far-field regime, as shown theoretically [3] and experimentally [4–9]. Furthermore, it could be shown experimentally and theoretically that near-field thermophotovoltaic conversion devices can be used to harvest this energy by transferring it towards a p-n junction [10,11]. Thanks to the tunneling of surface phonon polaritons (SPPs) supported by the primary source, this energy transfer is quasimonochromatic, which is very advantageous for the energy conversion with a photovoltaic cell [11]. However, recent theoretical works [12] have demonstrated the strong potential of near-field heat exchanges in the most general context of heat engines for capturing low-grade waste heat for power generation. Beside this result, a mechanism of photon-tunneling enhancement has been predicted in three-body (3B) systems [13–16] when passive relays are used to connect two bodies in interaction. In this paper, we study the thermodynamic performance of such a 3B system and demonstrate the strong potential of these near-field heat engines for energy harvesting.

The properties of the thermal radiation driving an energy-conversion process depend on the distribution and the number of bodies interacting with the converter. Let us compare the operating modes of two-body (2B) and 3B radiative heat engines, which are both sketched in Fig. 1. In a 2B heat engine, a hot source at temperature $T_h$ radiates towards a converter which is assumed to be in contact with a cold sink at temperature $T_c < T_h$. In the 3B configuration, a passive intermediate body of width $\delta$ is placed between the source and the sink. Note that this passive relay is maintained at the same separation distance $d$ from both the source and the sink as the cavity width in the 2B system. Hence, we do not introduce in the 3B heat engine an exaltation mechanism which results from a simple reduction of distances. Moreover, we assume that the intermediate body reaches a local equilibrium temperature $T_r$, an assumption that is justified in practical applications for the sizes of the body that we consider here. This temperature $T_r$ is not arbitrary. It is taken such that the net energy flux that the intermediate body exchanges with the hot and cold bodies vanishes. Hence, $T_r$ is an implicit function of $T_h$, $T_c$, and the two parameters $d$ and $\delta$ that specify the geometry of the problem. As a consequence, the energy flux radiated by the hot body coincides with the flux received by the cold body. This ensures that the energy supplied to the system comes only from the hot source, since, under these conditions, a thermostat at $T_r$ in contact with the passive relay will provide a vanishing net energy flux.

The planar 2B and 3B structures considered here have an infinite transversal extension. When all the bodies are separated by vacuum, the net energy flux on the cold body can be written as an integral over monochromatic radiation
The contributions of frequency $\omega$, which in the near-field regime is given by $\Phi_{iB} = \int_0^{\infty} \left( d\omega / 2\pi \right) \psi_{iB}(\omega, d, \delta)$ ($i = 2, 3$) with

$$\phi_{3B}(\omega, d, \delta) = \hbar \omega \sum_j \int_{c\omega>\omega} \frac{d^2 \kappa}{(2\pi)^2} \left[ n_{hr}(\omega) T_j^{hr}(\omega, \kappa, d, \delta) + n_{rc}(\omega) T_j^{rc}(\omega, \kappa, d, \delta) \right]$$

for the 3B configuration [14] and

$$\phi_{2B}(\omega, d, \delta) = \hbar \omega \sum_j \int_{c\omega>\omega} \frac{d^2 \kappa}{(2\pi)^2} n_{hc}(\omega) T_j^{hc}(\omega, \kappa, d, \delta)$$

in the 2B case [3,17]. Above, we have introduced $n_{\alpha}(\omega) = n_{\alpha}(\omega) - n_{\beta}(\omega)$, where $n_{\alpha}(\omega) = (e^{\hbar \omega / k_BT_a} - 1)^{-1}$ are the distributions of photons at equilibrium temperature $T_a$ with $\alpha = h, r, c$, $k_B$ being Boltzmann’s constant and $2\pi \hbar$ Planck’s constant. In Eqs. (1) and (2), the sum runs over the polarizations $j = s, p$, and the integration is carried out over the components of the transverse wave vector $\kappa = (k_x, k_y)$, with $\kappa = |\kappa| > \omega/c$, $c$ being the speed of light in vacuum. This means that only the dominant near-field contribution of evanescent waves is taken into account, whereas the contribution of the propagating modes with $\kappa < \omega/c$ is neglected. The transmission coefficients of the 2B and 3B systems are defined as [3,14,17]

$$T_j^{hr} = 4|\tau_j^h|^2 \Im(\rho_j^h) \Im(\rho_j^r) e^{-4|k_z|d} / |D_j^{hr}|^2,$$

$$T_j^{rc} = 4|\rho_j^r|^2 \Im(\rho_j^r) e^{-2|k_z|d} / |D_j^{rc}|^2,$$

$$T_j^{hc} = 4|\rho_j^r|^2 \Im(\rho_j^r) e^{-2|k_z|d} / |D_j^{hc}|^2,$$

where $k_z = \sqrt{\omega^2 / c^2 - \kappa^2}$ is the normal component of the wave vector while $D_j^{hr} = 1 - \rho_j^h\rho_j^r e^{2i k_z d}$, $D_j^{hr} = 1 - \rho_j^h\rho_j^r e^{2i k_z d}$, and $D_j^{hc} = 1 - \rho_j^h\rho_j^r e^{2i k_z d}$ are the Fabry-Pérot-like denominators. Here $\rho_j^r = \rho_j^r(\omega, \kappa)$, $\rho_j^r = \rho_j^r(\omega, \kappa)$, and $\rho_j^r = \rho_j^r(\omega, \kappa)$ are the reflection coefficients of the hot, intermediate, and cold bodies, respectively. $\tau_j^r = \tau_j^r(\omega, \kappa)$ are the transmission coefficients of the intermediate body, and $\rho_j^{hr} = \rho_j^r + (\tau_j^r)^2 \rho_j^r e^{2i k_z d} / |D_j^{hr}|$ are the reflection coefficients of the hot and the intermediate bodies considered as a single entity.

The expressions (3) for the transmission coefficients show that the three bodies are coupled together due to multiple interaction mechanisms resulting in their non-trivial optical properties. Moreover, in view of Eqs. (1) and (2), the energy flux $\Phi_{iB}$ can be written as a sum over the contributions stemming from the different constituents of the system which are in local thermal equilibrium, i.e., $\Phi_{iB} = \sum_{\alpha} \Phi_{iB}^{(\alpha)}(T_a)$ with $\alpha = h, c$ for 2B and $\alpha = h, r, c$ in the 3B case. The fluxes $\Phi_{iB}^{(\alpha)}(T_a)$ depend only on the local equilibrium temperatures $T_a$ of the constituents through the distribution functions $n_{\alpha}(\omega)$. Hence, the partial entropy fluxes $\Psi_{iB}^{(\alpha)}(T_a)$ carried by the thermal fields generated by the different constituents are given by [12]

$$\Psi_{iB}^{(\alpha)}(T_a) = \int_0^{T_a} d\omega \frac{d}{dT_a} \Phi_{iB}^{(\alpha)}(T).$$

Therefore, the net entropy flux on the cold body reads

$$\Psi_{iB} = \sum_{\alpha} \Psi_{iB}^{(\alpha)}(T_a) = \int_0^{\infty} \frac{d\omega}{2\pi} \Psi_{iB}(\omega, d, \delta).$$

where the spectral entropy fluxes take the form

$$\psi_{3B}(\omega, d, \delta) = k_B \sum_j \int_{c\omega>\omega} \frac{d^2 \kappa}{(2\pi)^2} \left[ m_{hr}(\omega) T_j^{hr}(\omega, \kappa, d, \delta) + m_{rc}(\omega) T_j^{rc}(\omega, \kappa, d, \delta) \right],$$

$$\psi_{2B}(\omega, d, \delta) = k_B \sum_j \int_{c\omega>\omega} \frac{d^2 \kappa}{(2\pi)^2} m_{hc}(\omega) T_j^{hc}(\omega, \kappa, d, \delta),$$

with $m_{\alpha}(\omega) = m_\alpha(\omega) - m_\beta(\omega)$ and $m_\alpha(\omega) = [1 + n_\alpha(\omega)] \ln [1 + n_\alpha(\omega) - n_\alpha(\omega)] n_\alpha(\omega)$. These last two relations are strictly valid only if the temperature dependence of the material properties of the constituents of the 2B or 3B system can be neglected in the considered range of working temperatures.

Once energy and entropy fluxes are known, the thermodynamics of the energy-conversion process can be analyzed as follows (the 3B and the 2B configurations will be discussed simultaneously). First of all, notice that, due to the difference of temperatures between the bodies, the transport of heat through the cavity proceeds irreversibly, and entropy is generated at a certain rate, say, $\Psi_{g}$. This entropy production $\Psi_{g}$ accounts for dissipative processes in
the thermalization of excited electrons at the surface of the cold body [18]. Since the bodies are thermalized, in particular, a heat flux \( \dot{Q} \) is transferred isothermally to the cold sink; we assume that this transference is done reversibly and, thus, \( \dot{Q} = T_c(\psi_{IB} + \psi_g) \). In this scheme, the heat engine can be considered as endoreversible, as discussed in Ref. [18] for the 2B problem in the far field. By taking into account the balances of energy and entropy fluxes, the work flux that can be delivered by the engine reads \( \dot{W} = \Phi_{IB} - T_c(\psi_{IB} + \psi_g) \). Since \( \psi_g \geq 0 \), the maximum work flux or thermodynamic availability is given by \( \dot{W}_{IB} \equiv \Phi_{IB} - T_c \psi_{IB} \). In addition, by considering \( \Phi_{IB} \) as the input energy flux, the efficiency of the engine is given by \( \eta_{IB} = \dot{W} / \Phi_{IB} \). According to this, an upper bound for the efficiency can be obtained by computing the ratio \( \tilde{\eta}_{IB} \equiv \dot{W}_{IB} / \Phi_{IB} \).

In the configuration we analyze, the hot and cold bodies are two 5-μm-thick silicon carbide (SiC) samples [19] that support a SPP with a resonance at \( \omega_{SPP} \approx 1.79 \times 10^{14} \text{ rad/s} \). Moreover, as in Ref. [14], we use in the 3B configuration for the intermediate slab a metallike medium which supports a surface mode (a plasmon) at the same frequency \( \omega_{SPP} \). Figure 2(a) shows the ratio of the maximum work flux in the 3B system to the maximum work flux in the 2B system, i.e., with and without an intermediate relay. It can be seen that a 3B engine can produce about 60% more work than a classical 2B system. If the width of the intermediate body becomes sufficiently large, the 3B interaction disappears (in the near-field regime), and both cavities, located between the source and the intermediate relay and between the relay and the sink, become independent. Then, the work production by the 3B heat engine becomes comparable to or even smaller than the one of a 2B engine. As for the efficiency of those engines, we see in Fig. 2(b) that they are comparable in both configurations provided the separation distances are large enough compared to the width of the intermediate slab. It is interesting to note that the 2B efficiency seems always to be larger than the 3B efficiency even in the parameter range where the extracted work of the 3B system exceeds that of the 2B system.

In order to get some insight on these results, we plot in Figs. 3(a) and 3(b) the transmission coefficients for \( p \)-polarized waves (the main contribution) in the \((\omega, \kappa)\) plane associated to the 3B engine by weighting them with the corresponding photon distribution functions. As a first observation, we see the presence of different surface-mode branches of the four coupled surface modes (symmetric and antisymmetric modes) in the 3B system [20] around the surface-mode resonance frequency of SiC. For these surface modes, the transmission is apparently high. These branches support high transmissions for large wave vectors, which means that a large number of modes contribute to the heat transfer in this spectral region [21,22]. The closer the frequency of the surface mode gets to Wien’s frequency of the heat source \( \omega_w = 2.82 k_B T_h / \hbar \), the higher the number of excitations that contribute to the transfer. Accordingly, if the hot body is cooled down to a temperature for which \( \omega_w \) is far from \( \omega_{SPP} \), the modes in the region around the SPP stop to contribute to the transfer, as can be seen in Fig. 3(b). The spectral energy fluxes plotted in Figs. 3(c) and 3(d) corroborate this tendency. Since the 3B photon-tunneling enhancement occurs in the SPP region, we thus observe in Fig. 3(c) an increase of the quasimonochromatic spectral energy flux \( \bar{\psi}_{3B} \) as compared with \( \bar{\psi}_{2B} \). Furthermore, the spectral entropy flux \( \bar{\psi}_{3B} \) and the spectral work flux \( w_{3B} \equiv \bar{\psi}_{3B} - T_c \bar{\psi}_{3B} \) are also peaked around the SPP frequency. As shown in Fig. 3(e), the negative entropic term drastically reduces the monochromatic contribution \( w_{3B} \) to the thermodynamic availability \( \dot{W}_{3B} (d, \delta) = \int_{-\infty}^{\infty} (d\omega / 2\pi) w_{3B}(\omega, d, \delta) \). This entropic term represents a non-negligible energy flux that the system transfers to the cold sink, thus diminishing the amount of usable work production.

Finally, we study the maximal work flux \( \dot{W}_{IB} \) that can be extracted from such a 3B heat engine compared with that of a 2B heat engine. To this end, we fix \( T_c = 300 \text{ K} \), while the temperature of the heat source \( T_h \) is varied. For the thickness of the vacuum gaps and the intermediate passive...
relay, we choose \(d = 100\text{ nm}\) and \(\delta = 133\text{ nm}\) for which \(\mathcal{W}_{3B}/\mathcal{W}_{2B}\) is maximum when \(T_h\) has reached a temperature of 400 K, as shown in Fig. 2(a) (in that case, the ratio \(\mathcal{W}_{3B}/\mathcal{W}_{2B}\) slowly increases for increasing \(T_h\)). The results are plotted in Fig. 4(a). They show that the discrepancy between \(\mathcal{W}_{3B}\) and \(\mathcal{W}_{2B}\) grows monotonically with respect to temperature while the 2B and 3B efficiencies remain very close to each other (\(\bar{\eta}_{2B} \geq \bar{\eta}_{3B}\)). In addition, the dependence of the work fluxes and efficiencies on the distance \(d\) for the optimal \(\delta\) are presented in Fig. 4(b), where the temperatures are set to \(T_h = 400\text{ K}\) and \(T_c = 300\text{ K}\). This example illustrates that in a 3B system the energy flux and the maximal work flux that can be extracted are enhanced by the interactions of the surface modes in the hot and cold body with that of the intermediate relay.

The maximum transfer in a 3B configuration takes place when the transmission coefficients attain their maximum value. The theoretical limit is thus achieved by the condition \(T_{ij}^{(hc)} = T_{ij}^{(rc)} = 1\), as also occurs for 2B systems \([21,23,24]\) when \(T_{ij}^{(hc)} = 1\). Using this in (1), (2), (6), and (7) and taking into account a cutoff wave vector \(\kappa_{c,IB} \gg \omega/c\), for which the modes are effectively confined, we get \(\Phi_i^{\max}_{IB} = \xi_i B(T_h - T_c^2)\) and \(\Psi_i^{\max}_{IB} = 2\xi_i B(T_h - T_c)\), where \(\xi_i B = \kappa_i^2 B k_i^2 / 24\hbar\). Notice that maximizing the energy flux implies also that the flow of entropy per channel is maximum \([23]\). The maximum work flux is thus \(\mathcal{W}_{3B}^{\max} = \mathcal{W}_{2B}^{\max} = \xi_i B(T_h - T_c)^2\), and in consequence the upper bound for the efficiency reads \(\bar{\eta}_{2B} \geq \bar{\eta}_{3B} = (T_h - T_c)/(T_h + T_c)\). Therefore, the efficiencies for the 2B and 3B systems are equal. However, we remark that the difference between a 3B and a 2B system is manifested through \(\kappa_{c,IB}\). The cutoff wave vector in a 3B system can be larger than that of the 2B configuration as shown in our numerical examples. Although the efficiencies and the ratios \(\Phi_i^{\max}_{IB}/\Psi_i^{\max}_{IB}\) are the same in the 3B and 2B system, it follows that

\[
\frac{\mathcal{W}_{3B}^{\max}}{\mathcal{W}_{2B}^{\max}} = \frac{\Phi_i^{\max}_{3B}}{\Phi_i^{\max}_{2B}} = \frac{\kappa_i^{2}_{c,3B}}{\kappa_i^{2}_{c,2B}} \geq 1. \tag{8}
\]

Hence, a larger maximum work flux in the 3B system is due to the larger energy flux which, in turn, results from the larger number of contributing modes.

For the general case of an \(N\)-body (NB) engine, we can always write the heat flux exchanged between the different parts of the system by using the Landauer formalism derived in Refs. \([21–23]\), the transmission coefficients being simply related to the scattering of the electromagnetic field radiated by each part of the system. In this case, a
suitable cutoff $\kappa_{c,NB}$ has to be considered. When $\kappa_{c,NB} > \kappa_{c,2B}$ for $N > 2$, an enhancement in the maximum work flux $\dot{W}_{NB}^{\text{max}}$ is thus expected with respect to the 2B case, while the efficiency $\bar{\eta}_{NB}^{\text{max}} = (T_h - T_c)/(T_h + T_c)$ remains the same for all $N$. Furthermore, the heat conductance in this NB endoreversible engine is, in general, nonlinear in the difference of temperatures $\Delta T = T_h - T_c$. However, the linear regime can be achieved if $\Delta T \ll T_h$, and, under this assumption, the efficiency becomes $\bar{\eta}_{NB}^{\text{max}} = \Delta T/(2T_h)$, which is half the Carnot efficiency. For engines with linear heat conductance such as the Novicov engine, the efficiency is given by

$$\bar{\eta} = \eta_{\text{CA}} = 1 - \sqrt{T_c/T_h} \quad [25], \quad \text{for} \quad \Delta T \ll T_h \quad \text{becomes} \quad \eta_{\text{CA}} = \Delta T/(2T_h).$$

We thus observe that the efficiency of our engine, in the appropriate limit, coincides with that of a Novicov engine.

In conclusion, we have demonstrated that the thermodynamic performance of 3B near-field heat engines can substantially overcome that of 2B systems. Our results pave the way for a generation of nanoscale energy converters driven by the physics of many-body interactions instead of the conventional two-body interactions. In addition, this work provides perspectives for investigating the thermodynamics of systems with long-range electromagnetic interactions.

This work was partially supported by the Spanish Government under Grant No. FIS2011-22603. I.L. acknowledges financial support through a FPI (Formación de Personal Investigador) scholarship (Grant No. BES-2012-054782) from the Spanish Government. J.M.R. acknowledges financial support from Generalitat de Catalunya under program ICREA (Institució Catalana de Recerca i Estudis Avançats) academia. P.-B.-A. acknowledges financial support from the CNRS (Centre National de la Recherche Scientifique) energy program.

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