Bose–Einstein oscillators and the excitation mechanism of free excitons in 2D layered organic–inorganic perovskites

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Following intense research on two-dimensional (2D) materials, there has been a resurgence of interest in 2D layered hybrid organic–inorganic perovskites. These 2D perovskites have direct band gaps regardless of their thickness. Excitons are confined to monolayers because of the materials’ self-organized quantum-well electronic structure. Gaining insight into the exciton dynamics is central to understanding the light–matter interactions in 2D organic–inorganic perovskites. Herein, we investigate the free-exciton dynamics in 2D layered CH3(CH2)2NH3PbI4 perovskite, demonstrating an anomalous temperature variation of the photoluminescence (PL) energy, which deviates from the conventional Varshni formula and is consistent with the behaviour of Bose–Einstein oscillators. The acoustic phonons induced by the coherent lattice motion of the atoms result in a positive temperature variation. Two-pulse emission modulation measurements reveal the excitation mechanism of the strong two-photon PL in CH3(CH2)2NH3PbI4 perovskite, in which two photons are simultaneously absorbed through a virtual state.

Introduction

Hybrid organic–inorganic CH3NH3PbX3 (X = I, Br, Cl) perovskites exhibit strong solar absorption, long electron–hole diffusion lengths and low trap densities.1,2 Thus, they show fascinating prospects for use in high-efficiency, low-cost solar cells.3–10 The efficiencies of such solar cells exceed 20%.11–13 All-inorganic halide perovskites (CsPbX3) synthesized in the form of colloidal quantum dots have also attracted intense interest because of their high quantum yields of up to 90%.14–17 To investigate the occurrence of two-dimensionally confined properties, ultra-thin CH3NH3PbX3 perovskite single-crystal flakes have been prepared through mechanical exfoliation,18 chemical vapour deposition (CVD)19,20 and solution self-assembly.21 The high crystal quality and symmetrical geometries of CH3NH3PbX3 perovskites result in high quality factors (Q), which can result in random lasing in whispering gallery mode. However, the crystal structure of a CH3NH3PbX3 perovskite is three-dimensional (3D) rather than layered (2D), and consequently, it is difficult to obtain CH3NH3PbX3 monolayers. Nonetheless, ultra-thin single-crystal CH3NH3PbI4 with a single unit cell of ~1.3 nm in thickness has recently been synthesized,22 and its photoluminescence (PL) peaks were found to exhibit a surprising dependence on the flake thickness.

The crystal geometries of organic–inorganic hybrid R(CH2)nNH3MX4 perovskites depend on the tolerance factor t, defined as $t = \sqrt{2(R_M + R_X)}/(R_{\text{RCH}_2\text{NH}_3} + R_X)$, where $R_{\text{RCH}_2\text{NH}_3}$, $R_M$ and $R_X$ are the ionic radii of the corresponding substances. In the case that the radii of the organic chain are larger than that of propylamine, an organic–inorganic hybrid R(CH2)nNH3MX4 perovskite will adopt a 2D layered structure.23 Hence, there are on-going efforts to develop 2D layered perovskites in the form of R(CH2)nNH3MX4 monolayers. Such 2D layered organic–inorganic halide R(CH2)nNH3PbX4 perovskite materials exhibit a self-organized quantum-well electronic structure (Fig. 1a), consisting of alternating ~0.6 nm inorganic layers and ~1 nm organic layers.24–26 They exhibit strong solar absorption, large exciton binding energies and small Bohr radii, which endow these R(CH2)nNH3PbX4 materials with excellent optical properties, such as sharp resonant emission with a narrow full width at half maximum (FWHM) and a high quantum yield.27 Previous reports have demonstrated that the PL peaks of R(CH2)nNH3MX4 perovskites can be tuned within the visible-infrared range by adjusting the organic component, R; the metal cation, M (M = Pb, Sn, Ge); and the halide, X (X = I, Br, Cl).28–30 Recently, single- and few-layer (C4H9NH3)2PbBr4 single-crystalline perovskite squares have been successfully prepared via a solution-
phase growth method. The optical band gap of the 2D square sheets was found to be slightly blue-shifted by 40 meV compared with that of the bulk crystal, but it was otherwise nearly indistinguishable for configurations ranging from 1 to 22 layers. In addition, mechanical exfoliation has been applied to produce 2D few-layer (C_6H_5C_2H_4NH_3)_2PbI_4 perovskites, in which strong anti-Stokes PL results in laser cooling by ~58.7 K. However, the nature of the excitons in 2D layered R(CH_2)_nNH_3MX_4 perovskites is still not well understood. Herein, we investigate the exciton dynamics in 2D layered CH_3(CH_2)_3NH_3PbI_4 perovskites in the range of 10–300 K by means of PL spectroscopy and two-pulse emission modulation (TPEM) spectroscopy. Interestingly, we find that the variation of the PL peak energy as a function of temperature deviates from Varshni’s empirical expression; the phase transition occurs in the range of 200–250 K. Below 200 K, the band gap energy first increases to a maximum of ~2.374 eV at 150 K but then monotonically drops to ~2.364 eV at 13 K as the temperature decreases. We demonstrate that Bose–Einstein oscillation contributes to the positive temperature variation of the PL peak energy as a result of free excitons. We also investigate the excitation mechanism of two-photon photoluminescence (TPPL), in which two photons are simultaneously absorbed through a virtual state to excite a single electronic transition. Our work reveals the mechanisms underlying exciton dynamics and excitation in 2D perovskites.

**Experiment**

**CH_3(CH_2)_3NH_3I synthesis and film preparation**

CH_3(CH_2)_3NH_3I was synthesized using the reported method. Briefly, 1.5 mL of CH_3(CH_2)_3NH_2 was added to 50 mL of ethanol under Ar gas and stirred for 30 min at 0 °C. Subsequently, 1 mL of hydroiodic acid (55 wt% in water, Sigma-Aldrich) was added. The mixed solution was stirred for a further 2 h. The white raw product CH_3(CH_2)_3NH_3I was obtained through rotary evaporation at 50 °C, washed three times with diethyl ether, and then finally recrystallized from a mixed solvent of diethyl ether and ethanol. The white solid was dried in vacuum for 24 h and stored in a glovebox. Then, 138 mg of PbI_2 and 105 mg of CH_3(CH_2)_3NH_3I were dissolved in 2.31 mL of DMF. A volume of 20 μL of the mixed solution was spin coated onto quartz with dimensions of 1 × 1 cm² at 2000 rpm for 2 min, and the samples were then placed in vacuum for 24 h for the removal of residual DMF solvent.

**TPPL measurements**

The TPPL spectra were measured using a home-built two-photon optical microscope. A mode-locked Ti:sapphire oscillator (TiF-100M, Avesta) was used as the excitation source, generating 80 fs pulses with a central wavelength of 785 nm and repetition rate of 84.5 MHz. The laser beam was passed through a 785/10 nm band-pass filter (LD01-785/10-25, Semrock), 5×
spatially expanded, and then reflected by a 50/50 beam splitter
to the objective lens (NA = 0.5). The emission signals were
collected by the same objective lens and filtered with two
785 nm notch filters [NF03-785E-25, Semrock] to reduce laser
scattering and with a long-pass filter with a cut-off wavelength
of 450 nm (Chroma) to remove the second-harmonic generation
signal. The spectra of the emission signals were measured using
a monochromator (Acton SpectraPro 2300i, Princeton Instruments)
coupled to a CCD (Pixis 100B, Princeton Instruments) via an optical fibre.

TPEM measurements

Two-pulse correlation measurements were performed using a
dual-channel regenerative amplifier (ORPHEUS Twins, Light
Conversion) pumped by a femtosecond laser oscillator
(PHAROS, Light Conversion). This system provided laser pulses
centred at 800 nm, with a pulse duration of 200 fs and a repeti-
tion rate of 1 MHz. The laser beam was split into two pulse
replicas. The two laser pulses were spatially overlapped and
focused by an objective (×20) onto the 2D perovskite thin film
(the laser pulses were broadened to ~330 fs after the objective).
The TPPL of the 2D perovskite thin film was collected using
the same objective and detected by a photomultiplier tube (ET17-63,
Hamamatsu). The emission was filtered using a 550 nm ±
50 nm band-pass filter and a 700 nm short-pass filters. The two-
pulse correlation curve was obtained by varying the time delays
between the two pulse replicas through a translational stage (M-
ILS250HA, Newport).

UV-vis absorption, PL, and AFM measurements

UV-vis absorption data for CH3(CH2)3NH3PbI4 were obtained
using a PerkinElmer LAMBDA 750 spectrophotometer. The
steady-state PL signal was recorded using a Witec Alpha 300R
confocal Raman microscope under 0.67 mW laser excitation at
4.88 eV. The samples were placed in a closed-cycle cryogenic
system for low-temperature measurements over a range of 10–
300 K. The AFM data were recorded using a BRUKER Dimension
FastScan system.

Results and discussion

CH3(CH2)3NH3I was synthesized through the reaction of CH3
(CH2)3NH3 and HI at 0 °C for 2 h and was then dissolved in
dimethylformamide (DMF) with PbI2 (10% wt). The as-grown
films were spin coated onto quartz at 2000 rpm for
2 min, and then dried under vacuum for 24 h. An AFM image
shows that the thickness of the 2D layered CH3(CH2)3NH3PbI4
films was ~80 nm (Fig. 1b). Fig. 1c displays the absorption and
PL spectra measured for the prepared 2D perovskite films at
room temperature. Two obvious absorption features are evident
at ~2.79 and ~2.43 eV, which are assigned as the band-edge
peak and the free-exciton peak, respectively. Intrinsic free-
exciton recombination dominates the PL emission, resulting
in a strong PL peak at ~2.38 eV under laser excitation at 2.63 eV
(Fig. 1c).

To further clarify the underlying dynamics responsible for
the evolution of the free-exciton emission, we plot the evolution
of the excitonic energy (normalized PL) as a function of the
temperature from 13 to 300 K under laser excitation at 4.88 eV,
as shown in Fig. 2a. Surprisingly, an anomalous non-monotonic
relationship between the PL peak energy and temperature is
observed for the 2D layered CH3(CH2)3NH3PbI4 films. As the
temperature decreases from room temperature, the PL peak
energy first increases from ~2.367 eV to a maximum of
~2.375 eV at 230 K, however sharply drops to ~2.373 eV at 200
K, which further increases to ~2.374 eV at 150 K and then
monotonically decreases to ~2.364 eV at 13 K (Fig. 2b). Typi-
cally, the PL peak energy monotonically increases as the
temperature decreases, as expressed by the Varshni model:\textsuperscript{43}

\[
E_\text{p}(T) = E_0 + \frac{aT^2}{T - \beta}.
\] (1)

where \(T\) is the temperature; \(E_\text{p}(T)\) and \(E_0\) are the fundamental
free-exciton emission energies at \(T = 0\) K, respectively; and \(a\) and \(\beta\) are constants. A monotonic increase in the PL peak
energy as the temperature decreases has been observed in many
semiconductor materials, such as GaN, InGaAs, MoS2, MoSe2,
and CdS.\textsuperscript{34-38} However, the Varshni model is not applicable for
our experimental data. The PL peak energy increase to a maximum at ~230 K as the temperature decreases, however,
which is similar in the range of ~230–205 K, and drops sharply
at 200 K. The full width at half maximum (FWHM) also show
a distinct and sharp variation at ~150 K, which decreases as the
temperature decrease in the range of 300–150 K, however,
become similar below 150 K (the inset in Fig. 2b).\textsuperscript{39} We assign
this behaviour to a phase transition of the perovskite crystal,
which have been observed in the 3D and 2D organic–inorganic
hybrid perovskites.\textsuperscript{40,41} It should be noted that the experimental
results cannot be fitted by Varshni model above 205 K, because
the two phases coexist within this temperature range. Surpris-
ingly, below 200 K, the PL peak energy first achieves a maximum
of 2.374 eV at 150 K and then monotonically decreases to
2.364 eV as the temperature decrease.

Generally, the temperature variation of the PL peak energy
has its origins in the effects of lattice thermal expansion (TE)
and electron–phonon interaction (EP), which, at constant
temperature, can be expressed as follows:\textsuperscript{42}

\[
(\Delta E_\text{p})_T = (\Delta E_\text{p})_{\text{EP}} + (\Delta E_\text{p})_{\text{TE}}
\] (2)

\((\Delta E_\text{p})_{\text{TE}}\) represents the harmonic corrections to the crystal
volume at low temperatures, which can be related to the
isotope masses through the zero-point vibrational amplitudes,
\((\Delta E_\text{p})_{\text{TE}}\) is usually much smaller than \((\Delta E_\text{p})_{\text{EP}}\), thus,
it is justifiable to neglect \((\Delta E_\text{p})_{\text{TE}}\) at low temperatures.\textsuperscript{43,44} We
focus on investigating the exciton dynamics below 200 K, and
suggest that the renormalization of the band gap and PL
emission stems from electron–phonon interactions that occur
below 200 K. In 2D layered perovskites, the valence bands (VBs)
consist mainly of the Pb(6s)\textsuperscript{2} and I(5p)\textsuperscript{6} orbitals, and
the conduction band (CB) is mainly composed of the Pb(6s)(6p)
orbital.\textsuperscript{45,46} The organic component does not play a significant
role in determining the electronic structure. The optical transitions in 2D perovskites thus stem from the 6s to 6p transition in Pb$^{2+}$, which is similar to that in PbI$_2$. Because Pb(207) has a larger atomic mass than I(126), the Pb atoms undergo Bose–Einstein oscillation at a low frequency that induces acoustic phonons, whereas the I atoms predominantly exhibit high-frequency Bose–Einstein oscillations, resulting in optical phonons. The electron–phonon interactions critically depend on the amplitudes of the phonons and the corresponding coupling constants. Thus, the temperature dependence of the free-exciton emission energy $E_g(T)$ should be related to that of both the optical phonon energy, $E_{OP}(T)$, and the acoustic phonon energy, $E_{AP}(T)$:

$$E_g(T) = E_0 + E_{OP}(T) + E_{AP}(T),$$

where $E_1$ and $E_2$ are the average energies of the Einstein oscillators corresponding to the optical and acoustic phonons, respectively; $A_1$ and $A_2$ describe the strength of the electron–phonon interactions, if negative, indicate that the band gap energy decrease with increasing temperature; $k_B$ and $T$ are the Boltzmann constant and temperature, respectively. Fig. 2b shows the fit of the experimental PL peak energy data to a model based on two types of Bose–Einstein oscillators (red dashed curve). The $E_0$ value obtained by fitting the data is $\sim$2.39 eV. The average energies of the optical ($E_1$) and acoustic ($E_2$) phonons are 27.5 meV and 0.028 meV, respectively, and $A_1$ and $A_2$ are $-32.3$ meV and 0.022 meV, respectively. Fig. 2c shows the energies of the optical and acoustic phonons as functions of temperature. The acoustic phonon function $E_{AP}$ is positive and monotonically increases with increasing temperature, whereas the optical phonon function $E_{OP}$ shows the opposite trend, monotonically decreasing as the temperature increases.

$$E_{OP}(T) = A_1 \left[ \frac{2}{\exp(E_1/k_B T) - 1} + 1 \right],$$

$$E_{AP}(T) = A_2 \left[ \frac{2}{\exp(E_2/k_B T) - 1} + 1 \right].$$
Moreover, |\(E_{\text{OP}}\) > |\(E_{\text{AP}}\)|. Thus, the total phonon function satisfies \((E_{\text{AP}} + E_{\text{OP}}) < 0\), resulting in an excitonic energy \(E_g(T)\) that is smaller than \(E_0\) and shows a non-monotonic variation. Thus, the coherent lattice motion of the atoms in 2D layered \(\text{CH}_3(\text{CH}_2)_3\text{NH}_3\text{PbI}_4\) films below 150 K induces acoustic phonons, resulting in an increase in the PL peak energy. However, the out-of-phase movements of the atoms in the lattice dominate above 150 K, giving rise to optical phonons and consequently causing the PL peak energy to decrease. Therefore, the temperature-dependent behaviour of the acoustic and optical phonons results in the non-monotonic temperature variation of the PL peak energy. Free excitons are confined in the quantum-well structure of 2D layered \(\text{CH}_3(\text{CH}_2)_3\text{NH}_3\text{PbI}_4\) perovskite, giving rise to a large exciton binding energy. Further analysis of the temperature dependence data yields insight into the free-exciton binding energy.

Fig. 2d shows the PL intensity as a function of \(1/T\) under laser excitation at 4.88 eV; the plot indicates that the PL intensity first gradually increases and then dramatically decreases as the temperature increases. Under steady-state excitation, the temperature dependence of the PL intensity can be expressed as:\textsuperscript{48}

\[
I(T) = \frac{I_0}{1 + \eta \exp(-E_B/k_B T)},
\]

where \(I(T)\) and \(I_0\) are the PL intensities of \(\text{CH}_3(\text{CH}_2)_3\text{NH}_3\text{PbI}_4\) at \(T\) and 0 K, respectively, and \(E_B\) is the exciton binding energy. By fitting the experimental data using eqn (6) (Fig. 2d) in the regions of 15–200 and 265–300 K, the exciton binding energy \(E_B\) is estimated to be \(\sim 282\) meV. This value is \(\sim 14.8\) times larger than that of 3D \(\text{CH}_3\text{NH}_3\text{PbI}_4\) (\(\sim 19\) meV),\textsuperscript{49} suggesting that the 2D material can be utilized as active elements for excitonic devices\textsuperscript{50,51} such as for excitonic energy transfer.\textsuperscript{52–54}

\(\text{CH}_3(\text{CH}_2)_3\text{NH}_3\text{PbI}_4\) exhibits excellent non-linear optical properties. A home-built two-photon optical microscope was used to investigate the TPPL of \(\text{CH}_3(\text{CH}_2)_3\text{NH}_3\text{PbI}_4\) perovskite.\textsuperscript{55}

Fig. 3 shows the one- and two-photon photoluminescence (OPPL and TPPL) spectra of the 2D layered \(\text{CH}_3(\text{CH}_2)_3\text{NH}_3\text{PbI}_4\) films under pulsed laser excitation at 3.1 and 1.55 eV. The PL intensity shows a linear relationship with the excitation power.
under optical pumping with 3.1 eV (Fig. 3a and b). Under 1.55 eV excitation, an exponential relationship between PL intensity and excitation power is observed, which can be well fitted using the function $y = ax^b$ (Fig. 3c and d), indicating the occurrence of TPPL. Considering the long tails of the absorption spectrum of the 2D layered CH$_3$(CH$_2$)$_4$NH$_2$PbI$_4$ films (Fig. 1c), two possible excitation mechanisms may be responsible for the TPPL, namely, a coherent two-photon absorption process or two sequential one-photon absorption processes. The schematic excitation diagrams of these processes are displayed in Fig. 4, respectively. In the coherent two-photon absorption model, two photons are absorbed simultaneously to drive a single electron from the VB into the CB via a virtual intermediate state (Fig. 4a). In the sequential one-photon absorption model, two photons are absorbed sequentially, mediated by a real intermediate state between the VB and CB (Fig. 4b).

To investigate the TPPL excitation mechanism of the 2D layered CH$_3$(CH$_2$)$_4$NH$_2$PbI$_4$ films, two-pulse emission modulation (TPEM) measurements were conducted to probe the correlated effects of two pulses on the observed PL emission. Two 1.55 eV femtosecond laser pulses with similar power were focused onto a 2D layered CH$_3$(CH$_2$)$_4$NH$_2$PbI$_4$ film with a good spatial overlap. The TPPL intensity was recorded as a function of the time delay ($\Delta t$) between the two laser pulses. In this configuration, the recorded TPPL emission has two possible origins: (1) two photons from the same laser excitation pulse and (2) two photons from different excitation pulses. It is easy to see that the contribution from the former process is independent of the time delay between two laser pulses, as the excitation photons originate from the same pulse. By contrast, the latter represents the cross-contribution of two individual laser pulses to the TPPL; thus, its contribution is maximal when the two pulses temporally overlap and decreases in intensity as they temporally separate. In the case of the coherent two-photon absorption model, the TPEM curve should show the same profile as that of the laser pulses because the emission originates from the simultaneous absorption of two photons through a virtual state. In the case of sequential one-photon excitations, the two one-photon excitation processes occur at the time scale of the lifetime of the real intermediate state; consequently, the TPEM dynamics should follow the lifetime of the intermediate state, similar to our previous reported TPPL excitation mechanism of gold nanorods. As shown in Fig. 4c, the measured TPEM curve of CH$_3$(CH$_2$)$_4$NH$_2$PbI$_4$ perovskite exhibits a FWHM of ~360 fs, which is consistent with the laser autocorrelation profile. These results suggest that the TPPL in CH$_3$(CH$_2$)$_4$NH$_2$PbI$_4$ perovskite is excited through the coherent two-photon absorption mechanism (Fig. 4a).

Conclusions

In 2D layered CH$_3$(CH$_2$)$_4$NH$_2$PbI$_4$ perovskite films, we observed a non-monotonic temperature variation of the PL peak energy in which the acoustic phonon energy exhibits a positive temperature variation, which is attributed to Bose–Einstein oscillation, whereas the optical phonon energy displays the opposite behaviour. The dielectric confinement effect due to the quantum-well structure of the material strengthens the Coulomb interaction between an electron and a hole, imparting the CH$_3$(CH$_2$)$_4$NH$_2$PbI$_4$ perovskite with a large exciton binding energy of ~282 meV and thus providing an opportunity to study the exciton dynamics. The nonlinear optical properties of TPPL in 2D layered CH$_3$(CH$_2$)$_4$NH$_2$PbI$_4$ perovskite were also observed, and we confirmed that the excitation is driven by a coherent two-photon absorption mechanism. The strong electron–phonon interactions and large exciton binding energy in 2D layered CH$_3$(CH$_2$)$_4$NH$_2$PbI$_4$ perovskite suggest its potential for use for high-efficiency excitonic energy transfer in lighting and display applications.

Author contributions

B. P. and K. P. L. conceived and supervised the experiment. B. P. synthesized CH$_3$(CH$_2$)$_4$NH$_2$PbI$_4$ perovskites. H. Z. and Q. X.
carried out two photon PL measurements and TPEM measurement. J. L., Y. L., L. B., H. L., J. X., L. D., L. Z., X. W. carried out the absorption and low temperature PL measurement. All authors discussed the results and wrote the manuscript.

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