Optimized Disk Layouts for Adaptive Storage of Interaction Graphs

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Abstract
We are living in an ever more connected world, where data recording the interactions between people, software systems, and the physical world is becoming increasingly prevalent. This data often takes the form of a temporally evolving graph, where entities are the vertices and the interactions between them are the edges. We call such graphs interaction graphs. Various application domains, including telecommunications, transportation, and social media, depend on analytics performed on interaction graphs. The ability to efficiently support historical analysis over interaction graphs requires effective solutions for the problem of data layout on disk. This paper presents an adaptive disk layout called the railway layout for optimizing disk block storage for interaction graphs. The key idea is to divide blocks into one or more sub-blocks, where each sub-block contains a subset of the attributes, but the entire graph structure is replicated within each sub-block. This improves query I/O, at the cost of increased storage overhead. We introduce optimal ILP formulations for partitioning disk blocks into sub-blocks with overlapping and non-overlapping attributes. Additionally, we present greedy heuristic approaches that can scale better compared to the ILP alternatives, yet achieve close to optimal query I/O. To demonstrate the benefits of the railway layout, we provide an extensive experimental study comparing our approach to a few baseline alternatives.

1 Introduction
We are living in an ever more connected world, where the data generated by people, software systems, and the physical world is more accessible than before and is much larger in volume, variety, and velocity. In many application domains, such as telecommunications, transportation, and social media, live data recording the interactions between people, systems, and the environment is available for analysis. This data often takes the form of a temporally evolving graph, where entities are the vertices and the interactions between them are the edges. We call such graphs interaction graphs.

Data analytics performed on interaction graphs can bring new business insights and improve decision making. For instance, the graph structure may represent the interactions in a social network, where finding communities in the graph can facilitate targeted advertising. In the telecommunications (telco) domain, call details records (CDRs) can be used to capture the call interactions between people, and locating closely connected groups of people can be used for generating promotions.

Interaction graphs are temporal in nature, and more importantly, they are append-only. This is in contrast to relationship graphs, which are updated via insertion and deletion operations. An example of a relationship graph is a social network capturing the follower-followee relationship among users. Examples of interactions...
graphs include CDR graphs capturing calls between telco customers or mention graphs capturing interactions between users of a micro-blogging service, like Twitter. The append-only nature of the interaction graphs make storing them on disk a necessity. Furthermore, the analysis of this historical interaction data forms an important part of the analytical landscape.

Since interaction graphs can potentially grow forever, they present a storage challenge for system designers. Even on modern servers with large amounts of memory, system designers cannot assume that the entire graph can fit. Instead, interaction graph systems must store their data on disk.

The ability to efficiently support historical analysis over interaction graphs requires effective solutions for the problem of data layout on disk. Most graph algorithms are characterized by locality of access [10], which is a direct result of the traversal-based nature of most of the graph algorithms. This is often taken advantage of by co-locating edges in close proximity within the same disk blocks [17]. This way, once a disk block is loaded into main memory buffers, several edges from it can be used for processing, reducing the disk I/O.

In interaction graphs, the locality of access is even more pronounced. First, the analysis to be performed on the interactions can be restricted to a temporal view of the graph, such as finding the influential users over a given week of interactions. This means that edges that are temporally close are accessed together. Second, traversals are again key to many graph algorithms, such as connected components, clustering coefficient, PageRank, etc. This means that edges that are close by in terms of the path between their incident vertices as well as their timestamps should be located together with the same blocks. In our earlier work [5], we introduced an interaction graph database that works on this principle of access locality. It uses a disk organization that consists of a set of blocks, each containing a list of temporal neighbor lists. A temporal neighbor list contains a head vertex and a set of incident edges within a time range. The layout optimizer aims at bringing together, into the same disk block, temporal neighbor lists that are (i) close in terms of their temporal ranges, (ii) have many edges between them, and (iii) have few edges going into temporal neighbor lists outside the block.

Many real world graph databases contain attributes. In the case of interaction graphs, the attributes can be considered as properties associated with the edges representing the interactions. Attributes can be stored in two ways, either separately (e.g., in a relational table), or locally with the temporal neighbor lists. If they are stored separately, then the graph database cannot take full advantage of locality optimizations performed for block organization. The database must go back and forth between the disk blocks to access the edge attributes. On the other hand, if attributes are stored locally in the disk blocks containing the graph structure, then there can be significant overhead due to disk I/O if only a few attributes are needed to answer a query.

To query an interaction graph, most algorithms traverse the graph structure to access the relevant attributes. Frequently, there are correlations among the attributes accessed by different queries. For example, queries $q_1$ and $q_5$ might access attributes $a_1$ and $a_2$, while queries $q_2$, $q_3$, and $q_6$ access attributes $a_3$ and $a_4$. Because interaction graphs are temporal, the co-access correlations for the attributes can vary for different temporal regions. Moreover, the co-access correlations might be unknown at the insertion time, but be discovered later, when the workload is known.

It is widely recognized that query workload and disk layout have a significant impact on database performance [2, 7, 18]. For table-based relational databases, this fact has led database designers to develop alternative approaches for storage layout: row-oriented storage [9] is more efficient when queries access many attributes from a small number of records, and column-oriented storage [1] is more efficient when queries access a small number of attributes from many records [18]. Unfortunately, although interaction graph databases, like relational databases, are the target of diverse query workloads, there is no clear correspondence to a row-oriented or column-oriented storage layout.

This paper presents an adaptive disk layout called the railway layout and associated algorithms for optimizing disk block storage for interaction graphs. The key idea is to divide blocks into one or more sub-blocks, where each sub-block contains a subset of the attributes (potentially overlapping), but the entire graph structure is replicated within each sub-block. This way, a query can be answered completely by only reading the sub-blocks that contain the attributes of interest, reducing the overall I/O.

There are a number of challenges in achieving an effective adaptive layout. First, we need to find the partitioning of attributes that minimizes the query I/O. To address this, we model the problems of overlapping and non-overlapping attribute partitioning as mixed-integer linear programs (ILPs), and provide optimal solutions that minimize the query I/O cost. Second, the query workload, and thus the attribute access pattern can change over time. For this purpose, our railway layout supports customization of the attribute partitioning of sub-blocks on a per-block basis. Third, such flexibility necessitates online configuration of attribute partitioning as the query workload evolves, which in turn requires fast algorithms for performing the attrib-
Figure 1: A partial example interaction graph for call data records, capturing the telephone calls among a set of people. To motivate our design, this paper will focus on a subgraph at a particular time range, indicated by the nodes colored white. Each edge in the graph is associated with attributes for the interaction, including the time the call was placed, the duration of the call, the cell phone tower, and the IMEI number identifying the device used.

ulte partitioning. For this purpose, we develop greedy heuristic algorithms for both overlapping and non-overlapping partitioning scenarios. These algorithms can scale to larger number of attributes, yet provide close to optimal query I/O performance. Finally, the railway layout trades off storage space to gain improved query I/O performance. The storage overhead is more pronounced for the case of overlapping partitioning. To address this, we limit the amount of storage overhead that can be tolerated, and integrate this limit to both our ILP formulations, as well as our greedy heuristics.

Our experiments demonstrate the benefits of the railway layout. For a storage increase of just 25%, the optimal overlapping partitioning algorithm reduces the query I/O cost by 45%. When allowed to double the storage usage, the overlapping partitioning algorithm can reduce the I/O cost by 73%. The heuristic algorithm performs almost as well, reducing the I/O cost by 72%, but reduces the running time needed to find a solution by orders of magnitude.

In summary, this paper makes the following contributions:

- We introduce the railway layout for adaptive organization of interaction graphs on disk.
- We introduce optimal ILP formulations for partitioning disk blocks into sub-blocks with overlapping and non-overlapping attributes, given a query workload. Our formulation also support upper bounding the amount of storage overhead introduced as a result of the railway layout.
- To support online adaptation, we develop greedy heuristics that can scale better compared to the ILP alternatives, yet achieve close to optimal query I/O.
- We provide an extensive experimental study comparing our approach to a few baseline alternatives.

The rest of the paper is organized as follows. Section 2 gives an overview of the railway layout in the context of an interaction database and motivates its design. Section 3 formalizes the optimal railway layout design problem. Section 4 gives Mixed Integer Linear Programming formulation of the optimal layout for overlapping and non-overlapping scenarios. Section 5 introduces our heuristic solutions for the same. Section 6 presents an experimental evaluation of our system. Section 7 discusses related work and Section 8 concludes the paper.

2 System Overview

The design of the railway disk layout builds on our prior work [5], which organized the disk layout for interaction graph databases to improve access locality. The railway layout extends the earlier design, by enabling
the system to adapt the layout to changing workloads, with the goal of reducing the disk I/O during querying, in exchange for a slight increase in the disk space used to store the graph.

2.1 Motivating Example

To explain the design of the railway layout, we first introduce a small, motivating example. Figure 1 shows a graph for the telephone call interactions among a set of people. Each node in the graph represents a person, and each edge in the graph represents a phone call from a caller to a callee. Each edge is associated with a set of attributes that maintain the details of the interaction, including the time the call was placed, the duration of the call, the cell phone tower, and the IMEI number identifying the device used to place the call. Thus, the schema for each edge is as follows:

\[
\text{call}(\text{time}, \text{duration}, \text{tower}, \text{imei})
\]

Recall that interaction graphs are append-only, and evolve over time. In other words, new timestamped edges are continuously added to the graph. For explanatory purposes, we focus on a subset of a graph at a particular time range. In the figure, the subset is indicated by the white nodes, and the edges between them. In this subset, there were four call interactions. One of them was a call from Alice to Bob, starting at 13:46. They spoke for 600 seconds. The call was received by cell phone tower 1, and the Alice’s phone had an IMEI number of 100.

A telecommunications company performs various analytics by processing the graph. For example, in order to understand how they should price their service plans, they might want to capture the duration of all calls for each user. To plan for infrastructure provisioning, they might want to record a count of the number of calls that each cell phone tower handled.

In an interaction graph, queries are associated with a time range, \([t_{\text{start}}, t_{\text{end}}]\). To answer queries, the graph database system must traverse the subgraph that contains edges with timestamp \(t\), such that \(t_{\text{start}} \leq t \leq t_{\text{end}}\). As the system traverses the graph, it reads the relevant attributes to answer the query. Note that a query might access all or some of the attributes. As concrete examples, imagine we have two queries. Query \(q_1\) asks for the average duration for calls from each tower. Query \(q_2\) asks for the count of calls made by each type of device. In other words we say that each query accesses a subset of the attributes:

\[
q_1 = \{\text{duration}, \text{tower}\}, q_2 = \{\text{imei}\}
\]

2.2 Storage for Locality

There are several ways in which one might store a graph on disk. The graph structure can be stored as a matrix representation or an adjacency list. Most graph databases choose an adjacency list representation because they reduce the storage overhead when graphs are sparse, and it is faster to iterate over the edges when traversing the graph. Attributes associated with each edge could be stored separately in a relational table, or along with the edges. Storing the attributes with the edges improves the locality, since the database can read the graph structure and associated attributes from the same disk block. To improve locality, typical disk layout schemes try to group as many adjacent nodes as possible in the same disk block.

Building on this basic design, our prior work \([5]\) extended the notion of locality to include a temporal dimension for handling interaction graphs. Nodes are placed in the same block if they are close together both spatially and temporally. Based on the edge timestamps, the adjacency lists are divided into multiple pieces and based on closeness of the nodes within the graph, these partial adjacency lists are combined into blocks. The locality of a block is determined by its conductance (i.e., the ratio of the number of dangling half edges), and its cohesiveness (i.e., a metric used to find highly connected components). Our earlier work describes a greedy algorithm for forming disk blocks with respect to this notion of locality.

Once the algorithm divides the graph into disk blocks, the graph data and attributes are stored in the layout scheme illustrated in the top of Figure 2. Note that this is an adjacency list representation in which attributes are stored with the edges. Each disk block contains a sequence of vertices, identified by a head-node id, followed by a count of the number of neighbors, and then the neighbor list itself. Each entry in the neighbor list is composed of a timestamp, an id for the destination vertex, and the properties for that edge. In the top of Figure 2, all of the information from the example interaction subgraph is stored in a single disk block.
2.3 Railway Layout

This paper introduces a new disk layout scheme, called the railway layout illustrated in the bottom of Figure 2. With the railway layout scheme, blocks are partitioned into sub-blocks, such that each sub-block contains the adjacency list representation from the original block, but only a subset of the attributes. The subset of attributes assigned to each sub-block is determined by the query workload.

For example, given queries q1 and q2, the railway layout would store the attributes time, duration, and tower in one sub-block, and the attribute imei in a second sub-block. In the ideal case, a query can be answered completely by reading a single sub-block that contains only the relevant information, and none of the irrelevant information, reducing the overall I/O cost. Of course, this layout comes at the expense of storage, as the graph structure information is duplicated in each sub-block. We argue that in general, I/O cost is more important than storage overhead, because a certain level of storage overhead can be accommodated by adding additional disks. In Sections 3 and 5, we will present our optimal and heuristic algorithms for discovering the sub-block partitions that keep the overhead below a user-specified threshold, while minimizing the disk I/O for the queries.

2.4 Adaptation

Because interaction graphs are append-only, and new edges are continuously added, there is a unique opportunity to adapt the disk layout with changing workloads over time. A database system utilizing the railway layout design would continually monitor the workload, and re-adjust the disk layout for historical data. This is illustrated in Figure 3. In the figure, we have an interaction graph with 4 attributes, namely a, b, c, and d. Initially, without any workload optimization, all disk blocks have a single sub-block that contains the entire set of attributes. This is shown in the upper half of the figure. After some time, the database adapts to the workload. This is shown in the lower half of the figure. We see that blocks from different time ranges have ad-
adapted differently, as the workload they observe is different. For instance, blocks $B_X$ and $B_Y$ were partitioned into two sub-blocks as $a, b, c - c, d$, whereas blocks $B_Z$ and $B_U$ were partitioned into three sub-blocks as $a - b, c - c, d$, and the blocks $B_V$ and $B_W$ stayed intact as $a, b, c, d$. A partition index is kept to track the partitioning of blocks in different time regions of the interaction graph database, which is shown on the right-hand side of the figure.

In the rest of this paper, we focus on the problem of how to determine the best partitioning for a given workload, which is the key capability that enables the adaptation. There are several other interesting challenges related to adaptation, including how to efficiently manage the partitioning index and how frequently to re-partition the disk layout. These topics are outside the scope of this paper.

3 Optimal Railway Design

The optimal railway design concerns the partitioning of disk blocks into sub-blocks such that the query I/O is minimized, while the storage overhead induced is kept below a desired threshold. This optimization is guided by the query workload observed by a disk block within a particular time range. Thus, the optimization problem is localized to individual disk blocks and the sub-blocks created could be potentially different for different disk blocks.

The partitioning of disk blocks into sub-blocks can be non-overlapping or overlapping. In the non-overlapping case, the attributes are partitioned among the sub-blocks with no overlap (i.e., a true partitioning). In the overlapping case, the subset of attributes contained within sub-blocks can overlap. In both cases, the complete graph structure for the block is replicated within the sub-blocks, which results in a storage overhead.

In both overlapping and non-overlapping partitioning, we trade increased storage overhead for reduced query I/O cost. In the overlapping case, the increase in the storage overhead is higher, as some of the attributes are replicated, in addition to the graph structure. On the other hand, enabling overlapping attributes is expected to reduce the query I/O (in the extreme case, there could be one sub-block per query). While the non-overlapping partitioning scenario is a special case of the overlapping one, specialized algorithms can be used to solve the former problem.

In the rest of this section, we first introduce basic notation and then formulate the overall optimization problem. The modeling of the query I/O and storage overhead are presented next, which complete the formalization of the optimal railway design problem.

3.1 Basic Notation

Let $Q$ be the query workload, where each query $q \in Q$ accesses a set of attributes $q.A$ and traverses parts of the graph for the time range $q.T = [q.t_s, q.t_e]$. Note that when we refer to a query, we mean query kind. That is, if $q_1$ is “all calls with a duration > 100” and $q_2$ is “all calls with a duration > 500”, then they are the same.
We denote the set of all attributes as \( A \). Given a block \( B \), we denote its time range as \( B.T \), which is the union of the time ranges of its temporal neighbor lists. Let \( s(a) \) denote the size of an attribute \( a \). We use \( c_e(B) \) to denote the number of temporal neighbor lists within block \( B \) and \( c_n(B) \) to denote the total number of edges in the temporal neighbor lists within the block. We overload the notation for block size and use \( s(B) \) to denote the size of a block \( B \). We have:

\[
s(B) = c_e(B) \cdot \left( 16 + \sum_{a \in B.A} s(a) \right) + c_n(B) \cdot 12
\]

(1)

Here, 16 corresponds to the cost of storing the edge id and the timestamp, and 12 corresponds to the cost of storing the head vertex (8 bytes) plus the number of entries (4 bytes) for a temporal neighbor list.

Our goal is to create a potentially overlapping partitioning of attributes for block \( B \), resulting in a set of sub-blocks denoted by \( \mathcal{P}(B) \). In other words, we have \( \bigcup_{B' \in \mathcal{P}(B)} B'.A = A \). Here, \( \mathcal{P} \) is the partitioning function.

### 3.2 Optimization Problem

We aim to find the partitioning function \( \mathcal{P} \) that minimizes the query I/O over \( B \), while keeping the storage overhead below a limit, say \( 1 + \alpha \) times the original. The original corresponds to the case of a single block that contains all the attributes. Let us denote the query I/O as \( I(\mathcal{P}, B) \) and the storage overhead as \( H(\mathcal{P}, B) \), our goal is to find:

\[
\mathcal{P} \leftarrow \arg\min_{\mathcal{P} : H(\mathcal{P}, B) < \alpha} I(\mathcal{P}, B)
\]

(2)

### 3.3 Storage Overhead Formulation

The storage overhead is defined as the additional amount of disk space used to store the sub-blocks, normalized by the original space needed by a single block (no partitioning). The storage overhead can be formalized as follows, for the non-overlapping case:

\[
H(\mathcal{P}, B) = (|\mathcal{P}(B)| - 1) \cdot \left( 1 - \frac{c_e(B) \cdot \sum_{a \in B.A} s(a)}{s(B)} \right)
\]

(3)

Basically, for the non-overlapping case, there is no overhead due to the attributes, as they are not repeated. However, there is overhead for the block structure that is repeated for each sub-block. There are \(|\mathcal{P}(B)| - 1\) such extra sub-blocks, and for each, the contribution to the overhead due to storing the graph structure is given by \( s(B) - c_e(B) \cdot \sum_{a \in B.A} s(a) \). Eq. 3 has one nice feature, that is, it does not depend on the details of the attribute partitioning, other than the number of partitions. We make use of this feature, later for the ILP formulation of the problem.

For the general case of a potentially overlapping partitioning, we can formulate the storage overhead as:

\[
H(\mathcal{P}, B) = \frac{\sum_{B' \in \mathcal{P}(B)} s(B')}{{s(B)}} - 1
\]

(4)

This formulation follows directly from the definition of storage overhead. While simple, it depends on the details of the partitioning, as \( s(B') \) is the size of a sub-block \( B' \), which depends on the list of attributes within the sub-block.

### 3.4 Query I/O Formulation

Let \( m \) be a function that maps a query \( q \) to the set of sub-blocks that are accessed to satisfy it for a relevant block \( B \) under a given partitioning \( \mathcal{P} \).

For the case of non-overlapping attributes, the \( m \) function lists all the sub-blocks whose attributes intersect with those from the query. Formally:

\[
m(\mathcal{P}, B, q) = \{ B' : B' \in \mathcal{P}(B) \land q.A \cap B'.A \neq \emptyset \}
\]

(5)

For the case of overlapping attributes, we use a simple heuristic to define the set of sub-blocks used for answering the query. Algorithm 1 captures it. The basic idea is to start with an empty list of sub-blocks and greedily add new sub-blocks to it, until all query attributes are covered. At each iteration, the sub-block that brings the highest relative marginal gain is picked. The relative marginal gain is defined as the total size of
the attributes from the sub-block that contribute to the query result, relative to the sub-block size. While computing
the marginal gain, attributes that are already covered by sub-blocks that are selected earlier are not considered.

| Algorithm 1: m-overlapping($\mathcal{P}, B, q$) |
|------------------------------------------------|
| **Data:** $\mathcal{P}$: partitioning function, $B$: block, $q$: query |
| $S \leftarrow \emptyset$; $R \leftarrow \emptyset$ |
| **while** $S \subset q, A$ **do** |
| $B' \leftarrow \arg\max_{B \in \mathcal{P}(B) \mid R} \sum_{a \in B', A \setminus S} \frac{c_i(B') \cdot (a)}{s(B')} \hspace{0.5cm} S \leftarrow S \cup B'.A$ |
| $R \leftarrow R \cup B'$ |
| **return** $R$ |

Given that we have defined the function $m$ that maps a query to the set of sub-blocks used to answer it, we can now formalize the total query I/O cost for a block under a given workload:

$$L(\mathcal{P}, B) = \sum_{q \in Q} w(q) \cdot 1(q.T \cap B.T \neq \emptyset) \cdot \sum_{B' \in m(\mathcal{P}, B, q)} s(B')$$  \hspace{0.5cm} (6)

We simply sum the I/O cost contributions of the queries to compute the total I/O cost. A query contributes to the total I/O cost if and only if its time range intersects with that of the block ($1(q.T \cap B.T \neq \emptyset)$). If it does, then we add the sizes of all the sub-blocks used to answer the query to the total I/O cost. Furthermore, we multiply the I/O cost contribution of a query with its frequency, denoted by $w(q)$ in the formula.

4 ILP Solution

In this section, we formulate the optimal railway design problem as a mixed Integer Linear Program (ILP). The main challenge is to represent the objective function and the constraint as a linear combination of potentially integer variables.

For the ILP formulation, we define a number of binary (0 or 1) variables:

- $x_{a,p}$: 1 if attribute $a$ is in partition $p$, 0 otherwise.
- $y_{p,q}$: 1 if partition $p$ is used by query $q$, 0 otherwise.
- $z_{a,p,q}$: 1 if partition $p$ is used by query $q$ and attribute $a$ is in partition $p$, 0 otherwise.
- $u_p$: 1 if partition $p$ is assigned at least 1 attribute, 0 otherwise.

Each of these variables serve a purpose:

- $x$s define the attribute-to-partition assignments.
- $y$s help formulate the query I/O contribution of each partition due to the graph structure they contain (excluding their assigned attributes).
- $z$s help formulate the query I/O contribution of each partition, only considering the attributes they are assigned.
- $u$s help formulate the storage overhead requirement.

In total, we have $|A| \cdot (|A| + 1) \cdot (|Q| + 1)$ variables. Here, we assume that the maximum number of partitions is fixed. In fact, we cannot have more partitions than attributes, so the number of partitions is upper bounded by $k = |A|$, and thus $0 \leq p < k$. However, some of these partitions can be empty in the optimal solution, which means that the number of partitions found by the ILP solution is typically lower than the maximum possible. A simple post-processing step removes empty partitions and creates the final partitioning to be used.

Finally, we define a helper notation for representing whether a variable is accessed by a query or not: $q(a) \equiv 1(a \in q.A)$.

We are now ready to state the ILP formulation. We separate the cases of non-overlapping and overlapping partitioning, as the former case can be formulated using smaller number of constraints.
4.1 Non-Overlapping Partitions

We start with the objective function, that is the total query I/O, which is to be minimized:

$$\sum_{q \in Q} w(q) \cdot \left( \sum_{p=1}^{k} (16 \cdot c_e(B) + 12 \cdot c_n(B)) \cdot y_{p,q} \right) + \sum_{a \in A} s(a) \cdot c_s(B) \cdot z_{a,p,q}$$

(7)

In Eq. 7, we simply sum for each query and each partition, and add the I/O cost of reading in the structural information found in a sub-block, if the partition is used by the query. We then sum over each attribute as well, and add the I/O cost of reading in the attributes. Note that $z_{a,p,q}$ could have been replaced with $x_{a,p} \cdot y_{p,q}$, but that would have made the objective function non-linear.

We are now ready to state our constraints. Our first constraint is that, each attribute must be assigned to a single partition. Formally:

$$\forall a \in A, \sum_{p=1}^{k} x_{a,p} = 1$$

(8)

Our second constraint is that, if a query $q$ contains an attribute $a$ assigned to a partition $p$, then partition $p$ is used by the query, i.e., $y_{p,q} = 1$. In essence, we want to state: $\forall \{p,q\} \in \{1..k\} \times Q, y_{p,q} = 1(\sum_{a \in A} q(a) \cdot x_{a,p} > 0)$.

In order to formulate this constraint, we use the following ILP construction: Assume we have two variables, $\beta_1$ and $\beta_2$, where $\beta_2 \in [0, 1]$ and $\beta_1 \geq 0$. We want to implement the following constraint: $\beta_2 = 1(\beta_1 > 0)$.

This could be expressed as a linear constraint as follows, where $K$ is a large constant guaranteed to be larger than $\beta_1$ for all practical purposes:

$$\beta_1 - \beta_2 \geq 0$$

$$K \cdot \beta_2 - \beta_1 \geq 0$$

(9)

We now apply this construction to our second constraint, where $\beta_1 = \sum_{a \in A} q(a) \cdot x_{a,p}$ and $\beta_2 = y_{p,q}$. This results in the following linear constraints:

$$\forall \{p,q\} \in \{1..k\} \times Q$$

$$\sum_{a \in A} q(a) \cdot x_{a,p} - y_{p,q} \geq 0$$

$$K \cdot y_{p,q} - \sum_{a \in A} q(a) \cdot x_{a,p} \geq 0$$

(10)

Our third constraint is that, if an attribute $a$ is assigned to a partition $p$, and partition $p$ is used by a query $q$, then the corresponding $z$ variable must be set to 1. That is, we want: $\forall \{a,p,q\} \in A \times \{1..k\} \times Q, z_{a,p,q} = 1(x_{a,p} = y_{p,q} = 1)$. We express this as a linear constraint, as follows:

$$\forall \{a,p,q\} \in A \times \{1..k\} \times Q$$

$$z_{a,p,q} - (x_{a,p} + y_{p,q}) \geq -1$$

(11)

In Eq. 11, when the $x$ and $y$ variables are both 1, the $z$ variable is simply forced to be 1. Otherwise, the $z$ variable can be either 0 or 1, but since the $z$ variables appear in the objective function as positive terms, the solver will set them to 0 to minimize the I/O cost (Note that the $z$ variables do not appear in any other constraint).

Our fourth constraint is that, if a partition is non-empty, then its corresponding $u$ variable must be set to 0. In other words, we want $\forall p \in \{1..k\}, u_p = 1(\sum_{a \in A} x_{a,p} > 0)$. This is expressed as linear constraints, as follows:

$$\forall p \in \{1..k\}$$

$$\sum_{a \in A} x_{a,p} - u_p \geq 0$$

$$K \cdot u_p - \sum_{a \in A} x_{a,p} \geq 0$$

(12)

Eq. 12 uses the same construction as the second constraint, where $\beta_1 = \sum_{a \in A} x_{a,p}$ and $\beta_2 = u_p$.

Our fifth, and the last, constraint deals with the storage overhead. We want to make sure that the storage overhead does not go over $a$. Recall that for the non-overlapping attributes case, the storage overhead
∀ \{ x \}_{a \in A}, \forall z \text{ partition must contain the attribute. I.e., we need to link the partition that is used by that query and that contains the attribute in question. Formally:}

\begin{equation}
\text{minimize } \sum_{q \in Q} w(q) \cdot \left( \sum_{p=1}^{k} (16 \cdot c_e(B) + 12 \cdot c_n(B)) \cdot y_{p,q} + \sum_{a \in A} s(a) \cdot c_e(B) \cdot z_{a,p,q} \right)
\end{equation}

subject to

\begin{align*}
\forall a \in A, \quad & \sum_{p=1}^{k} x_{a,p} = 1 \\
\forall [p,q] \in [1..k] \times Q, \quad & \sum_{a \in A} q(a) \cdot x_{a,p} - y_{p,q} \geq 0 \\
\forall [p,q] \in [1..k] \times Q, \quad & K \cdot y_{p,q} - \sum_{a \in A} q(a) \cdot x_{a,p} \geq 0 \\
\forall [a,q] \in A \times Q, \quad & z_{a,p,q} - (x_{a,p} + y_{p,q}) \geq -1 \\
\forall p \in [1..k], \quad & \sum_{a \in A} x_{a,p} - u_p \geq 0 \\
\forall p \in [1..k], \quad & K \cdot u_p - \sum_{a \in A} x_{a,p} \geq 0 \\
\sum_{p=1}^{k} u_p \leq 1 + \frac{\alpha}{1 - \frac{c_e(B) \sum_{a \in A} s(a)}{s(B)}}
\end{align*}

Figure 4: ILP formulation for the non-overlapping optimal railway design.

depends on the number of partitions used (Eq. 3). That means that the only ILP variables it depends on are the us. In particular, the number of partitions used is given by \( \sum_{p=1}^{k} u_p \). This results in the following linear constraint:

\begin{equation}
\sum_{p=1}^{k} u_p \leq 1 + \frac{\alpha}{1 - \frac{c_e(B) \sum_{a \in A} s(a)}{s(B)}}
\end{equation}

The final ILP formulation for the non-overlapping partitioning is given in Figure 4. We have a total of \(|A|^2 \cdot |Q| + 2 \cdot |A| \cdot |Q| + 3 \cdot |A| + 1\) constraints and the objective function contains \(|A| \cdot |Q| \cdot (1 + |A|)\) variables.

4.2 Overlapping Partitions

We present an ILP formulation of the problem, as we did for the case of non-overlapping partitions in Section 4.1. We use the same set of variables and the same objective function. However, the formulation of the constraints differ.

Our first constraint is that, each attribute must be assigned to at least one partition. Formally:

\begin{equation}
\forall a \in A, \sum_{p=1}^{k} x_{a,p} \geq 1
\end{equation}

As our second constraint, we require that for each attribute contained in a query, there needs to be a partition that is used by that query and that contains the attribute in question. Formally:

\begin{equation}
\forall [a,q] \in A \times Q, \sum_{p=1}^{k} z_{a,p,q} \geq q(a)
\end{equation}

As our third constraint, we require that if a query is using an attribute from a partition, then that partition must contain the attribute. I.e., we need to link the \( z \) variables with the \( x \) variables as \( \forall [a,q] \in A \times [1..k] \times Q, (z_{a,p,q} = 1) \Rightarrow (x_{a,p} = 1) \). This can be stated as linear constraints:

\begin{equation}
\forall [a,q] \in A \times [1..k] \times Q, x_{a,p} - z_{a,p,q} \geq 0
\end{equation}
As our fourth constraint, we require that if a query is using at least one attribute from a partition, then that partition must be used by the query. I.e., we need to link the \( z \) variables with the \( y \) variables as 

\[
\forall \{p,q\} \in \{1..K\} \times Q, \quad y_{p,q} = 1 \left( \sum_{a \in A} z_{a,p,q} > 0 \right).
\]

As before, we use the ILP construction from Eq. 9 for this, where \( \beta_2 = y_{p,q} \) and \( \beta_1 = \sum_{a \in A} z_{a,p,q} \). We get:

\[
\forall \{p,q\} \in \{1..K\} \times Q, \quad \sum_{a \in A} z_{a,p,q} - y_{p,q} \geq 0
\]

\[
\forall \{p,q\} \in \{1..K\} \times Q, \quad K \cdot y_{p,q} - \sum_{a \in A} z_{a,p,q} \geq 0
\]  \tag{17}

Our fifth constraint is that, if an attribute \( a \) is assigned to a partition \( p \), and partition \( p \) is used by a query \( q \), then the corresponding \( z_{a,p,q} \) variable must be set to 1. This is same as the formulation for the non-overlapping case from Eq. 11.

Our sixth constraint is that, if a partition is non-empty, then its corresponding \( u \) variable must be set to 0. Again, this is same as the formulation for the non-overlapping case from Eq. 12.

Our seventh, and the last, constraint deals with the storage overhead. However, the storage overhead formulation for the overlapping case is different from the one for the non-overlapping case. This is because the overhead does not merely depend on the number of partitions, as attributes might have to be read multiple times from different partitions (due to the overlaps). As a result, we express the overhead using base variables as in the objective function. Formally:

\[
\sum_{k=1}^{K} \left( 16 \cdot c_e(B) + 12 \cdot c_a(B) \right) \cdot u_p + \sum_{a \in A} s(a) \cdot c_e(B) \cdot x_{a,p} \leq s(B) \cdot (1 + \alpha)
\]  \tag{18}

The final ILP formulation for the overlapping partitioning is given in Figure 5. We have a total of \( 2 \cdot |A|^2 \cdot |Q| + 3 \cdot |A| \cdot |Q| + 3 \cdot |A| + 1 \) constraints and the objective function contains \( |A| \cdot |Q| \cdot (1 + |A|) \) variables.

5 Heuristic Solution

The ILP formulation described in Section 3 finds an optimal solution to the problem of partitioning disk blocks into sub-blocks such that the query I/O is minimized. Unfortunately, solving these types of constraint problems at scale can become a performance bottleneck, since integer programming is NP-Hard. In a graph database using the railway layout, the layout optimization of a block should be fast enough so that it could be piggybacked on disk I/O when significant workload change that necessitates a new layout is detected. We therefore introduce heuristic algorithms for both overlapping and non-overlapping partitioning scenarios. Experiments in Section 6 demonstrate that these heuristic algorithms show significantly improved running times over the optimal approaches, while still appreciably reducing the query I/O cost.

5.1 Non-Overlapping Attributes

For the non-overlapping attributes scenario, we use a heuristic algorithm that greedily assigns attributes to partitions. The pseudo-code of it is given in Algorithm 2. One complication is that, the number of partitions is not known a priori. Yet, we know that the number of partitions is bounded by the number of attributes. As such, we start with a single partition, and try different number of partitions, until we hit the maximum number of partitions or the storage overhead goes beyond the threshold \( \alpha \). Among all partition counts tried, the one that provides the lowest query cost is selected as the final partitioning. Note that, for the non-overlapping scenario, the storage overhead is an increasing function of the number of partitions. As such, once we exceed the storage overhead threshold, we can safely stop trying larger numbers of partitions.

For a fixed number of partitions, the algorithm operates by incrementally assigning attributes to partitions. We consider the attributes in decreasing order of their frequency. This is because the reverse, that is assigning highly frequent attributes later, may result in making assignments that are hard to balance out later. Initially, all partitions are empty. We pick the next unassigned attribute and evaluate assigning it to one of the available partitions. The assignment that results in the lowest query cost is selected as the best assignment and is applied. When computing the query cost, we only consider the attributes assigned so far.
Algorithm 2: Algorithm for partitioning blocks into sub-blocks with non-overlapping attributes.

Data: $B$: block, $Q$: set of queries
$c^* = \infty$

for $k = 1 \text{ to } |A|$ do

\[ R[i] \gets \emptyset, \forall i \in [1..k] \]

for $a \in A$, in decr. order of $f(a)$ do

\[ c \gets \infty \]

\[ j \gets -1 \]

for $i \in [1..k]$ do

\[ R[i] \leftarrow R[i] \cup \{a\} \]

if $L(R, B, Q) < c$ then

\[ c \leftarrow L(R, B, Q) \]

\[ j \leftarrow i \]

\[ R[i] \leftarrow R[i] \setminus \{a\} \]

\[ R[j] \leftarrow R[j] \cup \{a\} \]

if $H(R, B, Q) > \alpha$ then break;

if $L(R, B, Q) < c^*$ then

\[ c^* \leftarrow L(R, B, Q) \]

\[ \mathcal{P}(B) \leftarrow R \]

return $\mathcal{P}(B)$

\[ \begin{align*}
\text{minimize} & \quad \sum_{q \in Q} w(q) \cdot \left( \sum_{p=1}^{k} \right) (16 \cdot c_e(B) + 12 \cdot c_n(B)) \cdot y_{p,q} \\
\text{subject to} & \quad \sum_{a \in A} x_{a,p} \geq 1 \\
& \quad \forall [a,q] \in A \times Q, \sum_{p=1}^{k} z_{a,p,q} \geq q(a) \\
& \quad \forall [a,p,q] \in A \times [1..k] \times Q, x_{a,b} - z_{a,p,q} \geq 0 \\
& \quad \forall [p,q] \in [1..k] \times Q, \sum_{a \in A} z_{a,p,q} - y_{p,q} \geq 0 \\
& \quad \forall [p,q] \in [1..k] \times Q, K \cdot y_{p,q} - \sum_{a \in A} z_{a,p,q} \geq 0 \\
& \quad \forall [p,q] \in [1..k] \times Q, z_{a,p,q} - (x_{a,p} + y_{p,q}) \geq 0 \\
& \quad \forall p \in [1..k], \sum_{a \in A} x_{a,p} - u_p \geq 0 \\
& \quad \forall p \in [1..k], K \cdot u_p - \sum_{a \in A} x_{a,p} \geq 0 \\
& \quad \sum_{p=1}^{k} (16 \cdot c_e(B) + 12 \cdot c_n(B)) \cdot u_p \\
& \quad + \sum_{a \in A} s(a) \cdot c_e(B) \cdot x_{a,p} \leq s(B) \cdot (1 + \alpha)
\end{align*} \]

Figure 5: ILP formulation for the overlapping partitioning
The computational complexity of the algorithm is $O(k^2 \cdot |A| \cdot |Q|)$, where $k$ is the maximum number of partitions tried. The $|Q|$ term is the number of unique queries and comes from the cost of computing the query I/O (this can be computed incrementally, even though this is not shown in the pseudo-code). While in the worst case we have $k = |A|$, resulting in a computational complexity of $O(|A|^3 \cdot |Q|)$, in practice $k$ is much lower due to the upper bound $a$ on the storage overhead.

5.2 Overlapping Partitions

For the overlapping attributes scenario, we use a heuristic algorithm that starts with each query in its own partition and greedily merges partitions until the storage overhead is below the limit. The pseudo-code of it is given in Algorithm 3.

We start the algorithm in a state where for each unique query there is a separate sub-block that contains the attributes from that query. If there are attributes not covered by the queries, they are assigned to a special sub-block. This is the “ideal” partitioning, because the I/O cost would be minimized for the workload at hand. However, in most practical settings, this partitioning will have excessive storage overhead. Thus, we iteratively combine the pair of partitions that has the lowest cost. This is repeated until the storage overhead is below the threshold $a$. The end result is the final overlapping partitioning.

We define the cost of a merge based on the query I/O and storage cost. In particular, we measure the increase in the query I/O due to the merge, per reduction in the storage space used. We want to minimize this metric. More formally, assuming $\mathcal{P}$ is the partitioning before the merge and $\mathcal{P}'$ is the partitioning after the merge, the utility can be formulated as:

$$\frac{L(\mathcal{P}', B, Q) - L(\mathcal{P}, B, Q)}{H(\mathcal{P}, B) - H(\mathcal{P}', B)}$$

Computational Complexity  The computational complexity of the algorithm is $O(|A| \cdot |Q|^3)$. At each iteration, the algorithm reduces the number of partitions by one and initially there are $|Q|$ partitions. As such, in the worst case, there will be $|Q|$ iterations. The number of pairs considered is bounded by $|Q|^2$. The utility metric can be computed incrementally, but requires iterating over the query attributes, bringing in the $|A|$ term.

6 Evaluation

In this section, we describe our prototype implementation, and the results of our evaluation, demonstrating that the railway layout scheme significantly reduces query I/O for interaction graphs.
To evaluate our design, we also implemented a workload simulator, whose parameters represent queries and disk-blocks. To solve the ILP formulation of the partitioning problem, it relies on the C libraries from the Gurobi Optimizer.

We have implemented the four partitioning algorithms described in this paper, and a workload simulator to evaluate the algorithms and our disk layout design. All source code for the algorithms, as well as the simulator and experiments are publicly available.\(^1\)

The partitioning algorithms were written in C++ using the LLVM 3.5 compiler. The implementation uses data structures from the graph database implementation described in our prior work \cite{PriorWork} to represent queries and disk-blocks. To solve the ILP formulation of the partitioning problem, it relies on the C libraries from the Gurobi Optimizer \cite{Gurobi} software.

To evaluate our design, we also implemented a workload simulator, whose parameters and default settings are given in Table 1. The default number of attributes in the graph database schema is taken as 10, even though we experiment with a range of values for it. The size of the attributes come from

\(^1\)https://github.com/usi-systems/graphdb
Parameter & Default
--- & ---
# of attributes & 10
attribute sizes & Zipf($z = 0.5, \{4, 1, 8, 2, 16, 32, 64\}$)
query length & Normal($\mu = 3, \sigma = 2.0$)
# of query kinds & 5
query kind freq. & Zipf($z = 0.5, n = 5$)
storage ohd. threshold & $\alpha = 1.0$

Table 1: Workload generation parameter defaults

the list of sizes given in Table 1 and are picked randomly from a Zipf distribution with $z = 0.5$. The average number of unique query types we have in the workload for a particular time point is taken as 5, which is another parameter we vary throughout our experiments. The frequencies of different queries follow a Zipf distribution with $z = 0.5$.

6.2 Environment
We ran all experiments on a machine with a 2.3 GHz Intel i7 processor that has 32 KB L1 data, 32 KB L1 instruction, 256 KB L2 (per core), 6 MB L3 (shared) cache, and 16 GB of main memory. The processor has four cores, but our implementation only uses a single core. The operating system was OS X 10.9.4.

6.3 Experiments
Our experiments evaluate three aspects of our design: (i) the reduction in query I/O due to using the railway layout, (ii) the expected increase in storage cost resulting from the railway layout, and (iii) the scalability of the partitioning algorithms.

We measured these three respective values, query I/O cost, storage overhead, and running time, for each partitioning algorithm, as we varied three parameters to the default workload in Table 1:

- **Number of attributes** is the total number of attributes in the iteration graph schema. We increased the attribute count by multiples of two from 2 to 16.
- **Number of query kinds** is the number of unique query types in the workload. We increased the number of query types by multiples of two from 2 to 14. Beyond 14, the optimal solvers were no longer able to find solutions in a reasonable amount of time.
- **Storage overhead threshold** is the user-specified parameter that dictates how much storage overhead will be tolerated for a solution. We increased the storage overhead threshold by increments of 0.25 from 0 to 2.0.

For all experiments, other than the experiment in which we explicitly altered the value, we used a default storage overhead threshold value of 1.0. We believe this is a reasonable number, as it corresponds with doubling the available storage space.

As baseline comparisons, we also measured the results for two naïve partitioning schemes: SinglePartition places all attributes into a single partition, and PartitionPerAttribute creates a separate partition for each attribute. The SinglePartition scheme represents the standard disk layout, and the PartitionPerAttribute approach represents an extreme partitioning (although not an optimal one, as it potentially increases both the query I/O and storage costs).

For each configuration, we ran the experiment 10 times. Each partitioning algorithm used the same workload for each run, but each run was on a different random workload using the same configuration parameters. We report the average (arithmetic mean) and standard deviation.

Query I/O Figure 6 shows the results from the query I/O cost measurements. In all three experiments, we see the benefit of the railway layout. The SinglePartition and PartitionPerAttribute layouts represent baseline measurements for a traditional layout and pathological partitioning scheme. All versions of the railway layout result in better query I/O than the baseline measurements, except when the storage threshold is set to not allow any overhead (as we would expect).
In the left graph, we see that the benefits of the railway layout become more pronounced as we increase the number of attributes. At the low end of the graph, with a schema of only 2 attributes, the optimal overlapping partitioning algorithm results in a 7 percent reduction in query I/O cost. However, at the high end, with 16 attributes, there is a 73 percent reduction in I/O cost. Note that the heuristic overlapping is almost as good, giving a 72 percent reduction in I/O cost.

In the middle figure, we see that the benefits of the railway layout remain relatively constant as we increase the number of query kinds. In the 2 query case, we see a 59 percent difference between the optimal overlapping and single partitioning schemes, while at the 14 query case, we see a 53 percent difference. While increasing the number of query kinds did not have a big impact on query I/O, it did have a large impact on running time, as we will see.

The railway layout makes a tradeoff between query I/O cost and storage cost. We see in the right graph of Figure 6, when the user explicitly disallows any increase in storage (i.e., sets the threshold to 0), then the railway layout does not help. However, with even just a slight 25 percent increase in storage, all railway layouts reduce query I/O, demonstrating reductions of 45 percent.

Storage Overhead  The experiments in Figure 7 quantify the storage overhead that one can expect with using the railway layout. In the left graph, we see that the optimal overlapping and heuristic overlapping approach the user specified limit of doubling the storage space. As expected, the algorithms will make use of extra storage in order to reduce the query I/O cost. The non-overlapping schemes are limited in the amount or storage overhead that they use, since they cannot duplicate attributes in separate partitions. So, the extra storage overhead is attributed to duplicating the graph structure.

The middle graph shows a similar result. The overlapping partitioning algorithms approach the user specified threshold, while the non-overlapping schemes are bounded.

The right graph in Figure 7 is interesting. It shows that as the user increases the threshold to a value of 2.0 (i.e., tripling the available storage) both optimal schemes will try to take advantage of the extra space to reduce query I/O.

Scalability  The experiments in Figure 8 show the running times for our four algorithms. As we can see in the left graph, when the schema had 14 attributes. The optimal overlapping scheme took 3.64 seconds to find a solution, and the optimal non-overlapping took 1.22 seconds. In contrast, both heuristic solutions took deciseconds (i.e., 1/10s of a second) to solve.

The number of query kinds had a large impact on solving time. After leaving the experiment running for more than 12 hours, we were not able to complete the optimal overlapping measurement for the case of 16 query kinds. This experiment demonstrates the benefit of our heuristic greedy algorithms.

However, as shown in the right graph, the storage overhead threshold did not have a significant impact on the running time. This is as expected, since the optimal solvers scale with the number of variables in the constraint problem, and the number of variables does not increase as we alter the storage overhead threshold.

Summary  Overall, our experiments demonstrate the benefits of the railway layout. For a storage increase of just 25%, the optimal partitioning algorithm reduces the query I/O cost by 45%. When allowed to double the storage usage, the overlapping partitioning algorithm can reduce the I/O cost by 73%. The heuristic algorithm performs almost as well, reducing the I/O cost by 72%, while also reducing the running time needed to find a solution by orders of magnitude.

7 Related Work

There has recently been increased research interest in large-scale graph analysis and programming models. These include synchronous vertex programming pioneered by Pregel [15], such as Apache Giraph [3]; asynchronous vertex programming pioneered by GraphLab [6, 14], and generalized iterated matrix-vector multiplication pioneered by PEGASUS [12]. These systems largely focus on the problem on analytical processing, while our work focuses on data management. Moreover, the graphs these systems provide do not have a temporal dimension.

The railway layout and algorithms build on our prior work [5], which added a temporal dimension to the notion of locality for organizing the disk layout of interaction graph databases. Graph database nodes are
placed in the same disk block if they are close together both spatially and temporally. The railway layout extends this design to partition disk blocks into sub-blocks that reduces the query I/O cost. Because interaction graphs are append only, the railway design enables the disk layout to adapt with changing workloads.

Our adaptation scheme is similar to work on adaptive layouts for relational database. The $H_2O$ [2] system can adapt its data layout into three types, row-major, column-major, or groups of columns, depending on the workload. HYRISE [7] provides a similar adaptive layout scheme for an in-memory relational database. Both systems use heuristic, iterative solutions to determine partitioning. The railway layout scheme differs, in that it targets interaction graphs, and we present optimal solutions, in addition to heuristic solutions.

The rise in popularity of social networks, and the recognition that workloads for social network data differ from traditional workloads, has lead to increased scrutiny on the problem of disk layout for graph databases. Bondhu [10], the layout manager for the Neo4j graph database [16], aims to minimize the number of seek operations for small user block sizes by fetching multiple friends’ data at the same time, and by clustering related data into the same block. Bondhu differs from our work in that the cost model does not include a notion of time, nor does it allow for adaptive layouts.

Instead of storing graph data with an adjacency list representation, GBase [11] uses a sparse matrix format. The matrix representation allows GBase to use compression schemes to store homogenous regions of graphs, significantly reducing the storage overhead for large graphs. On top of this storage layout, GBase provides a parallel indexing mechanism that accelerates queries. While the high-level motivations of GBase (i.e., improving query response time for graph database queries) are similar to our work, they are largely focused on the storage overhead. In contrast, we focus on reducing the query I/O cost.

DeltaGraph [13], like our work, includes a temporal component to the layout design, to efficiently support queries over historical graph data. DeltaGraph differs from our work in that they are targeting distributed graph databases, that partition data across a set of machines. Consequently, they propose a quite different cost model. Moreover, our railway design lays the foundation for an adaptive disk layout mechanism, which can change over time. Since the DeltaGraph mechanism is static, we expect that the two designs are complementary.

Finally, there is prior work on temporal RDF databases, which aims to improve the response time of SPARQL queries. Notably, Bornea et al. [4] describe a way of mapping an RDF store to a relational database, in order to leverage the overwhelming amount of work on relational database query optimization. Their work is similar to ours in that they use a ILP formulation of a constraint problem in order to optimally determine data placement.

8 Conclusion

Many of today’s most popular applications rely on data analytics performed on Interaction graphs. The ability to efficiently support historical analysis over interaction graphs require effective solutions for the problem of data layout on disk. In this paper, we have presented a novel disk layout design for graphs called the railway layout. The design is analogous to hybrid column and row stores in relational databases. Our simulations show that the railway layout significantly reduces query I/O cost for randomized workloads. We have identified the key challenge for systems to implement the railway layout, which is how to partition blocks into sub-blocks. To solve that problem, we first presented optimal solutions for overlapping and non-overlapping partitioning using an ILP formulation. To improve the scalability of the partitioner, and enable future work in online adaptation of the disk layout, we have also presented heuristic greedy algorithms that find results close to the optimal solutions, but exhibit faster running times on large graph schemas and workloads. To compare the four partitioning algorithms, we have presented a number of experiments that evaluate the effectiveness and tradeoffs of the various approaches. Overall, the railway layout design appreciably improves the performance of data analytics on interaction graphs, and lays the ground work for future systems design research.

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