A simple method to combine multiple molecular biomarkers for dichotomous diagnostic classification

Manju R Mamtani†1, Tushar P Thakre*1,2, Mrunal Y Kalkonde1, Manik A Amin1, Yogeshwar V Kalkonde1, Amit P Amin1 and Hemant Kulkarni†1

Address: 1Lata Medical Research Foundation, Nagpur, India and 2University of North Texas Health Science Center, Fort Worth, Texas, USA

Email: Manju R Mamtani - mamtani@uthscsa.edu; Tushar P Thakre* - tthakre@hs.c.unt.edu; Mrunal Y Kalkonde - mkalkonde@yahoo.com; Manik A Amin - saiamin2004@yahoo.com; Yogeshwar V Kalkonde - yvkalkonde@yahoo.com; Amit P Amin - amit_p_amin@yahoo.com; Hemant Kulkarni - hemant_kulkarnius@yahoo.com

* Corresponding author †Equal contributors

Background: In spite of the recognized diagnostic potential of biomarkers, the quest for squelching noise and wringing in information from a given set of biomarkers continues. Here, we suggest a statistical algorithm that – assuming each molecular biomarker to be a diagnostic test – enriches the diagnostic performance of an optimized set of independent biomarkers employing established statistical techniques. We validated the proposed algorithm using several simulation datasets in addition to four publicly available real datasets that compared i) subjects having cancer with those without; ii) subjects with two different cancers; iii) subjects with two different types of one cancer; and iv) subjects with same cancer resulting in differential time to metastasis.

Results: Our algorithm comprises of three steps: estimating the area under the receiver operating characteristic curve for each biomarker, identifying a subset of biomarkers using linear regression and combining the chosen biomarkers using linear discriminant function analysis. Combining these established statistical methods that are available in most statistical packages, we observed that the diagnostic accuracy of our approach was 100%, 99.94%, 96.67% and 93.92% for the real datasets used in the study. These estimates were comparable to or better than the ones previously reported using alternative methods. In a synthetic dataset, we also observed that all the biomarkers chosen by our algorithm were indeed truly differentially expressed.

Conclusion: The proposed algorithm can be used for accurate diagnosis in the setting of dichotomous classification of disease states.

Background
In spite of a plethora of available choices [1-4] to statistically analyze the high-dimension data derived from gene microarrays or serum proteomic profiles, a single method of choice remains elusive. Two main objectives motivate such analyses: first, to identify novel biomarkers that characterize specific disease states so as to gain biological and therapeutic insights and second, to identify patterns of expression that will discriminate among disease states and aid in diagnostic classification. Clearly, the statistical
methods suited to achieve one objective may differ from the methods appropriate for the other purpose – not only in terms of the procedural assumptions and details but also in terms of the results. Several extensive reviews deal with this issue [1,5-10].

For the purpose of diagnostic classification using biomarker data, a common statistical option is to use linear discriminant functions [11,12]. However, this choice is not straightforward because of an important asymmetric disposition of the typical datasets. For example, the number of biomarkers (usually several thousands) greatly exceeds the number of samples (usually in hundreds or less). Each biomarker, therefore, must be assessed for its potential association with the disease status leading to a problem of multiple comparisons [13]. Consequently, while on the one hand a few highly significant associations may mask other important associations; on the other hand noisy, false positive associations can be detected. A successful use of linear discriminant analyses therefore rests on a proper choice of a finite but informative subset of the biomarkers.

A natural approach to supervised diagnostic classification using such datasets would be to assume expression of each biomarker as a diagnostic test [14,15]. Since the expression levels of many of the biomarkers can be expected to be correlated with each other [15], the problem in diagnostic classification is that of finding an optimum combination of the correlated diagnostic tests that will maximize the discriminatory performance. The formal optimization methods available for this problem are however constrained to a limited number of diagnostic tests [16] An analysis of a dataset of n biomarkers will need to consider a total of 2 to the n-1 combinations of the biomarkers, which can demand immense computation time in the context of the microarray experiments. We believe, however, that a simpler solution to this problem exists, which can be arrived at by using classical statistical techniques. Here, we suggest a statistical algorithm to circumvent these problems of data dimension and asymmetry and using four datasets of differing nature demonstrate the use of the proposed technique for the purpose of dichotomous diagnostic classification.

Results

Proposed statistical algorithm

Contingent upon the assumption that each biomarker can be considered as a diagnostic test, we propose a three-step procedure (Fig. 1) to arrive at an optimum combination of the biomarkers that will have a high degree of diagnostic accuracy. The proposed algorithm consists of three steps: screening the biomarkers individually based on the Performance Index (PI) which is a function of the estimated area under the receiver characteristic curve (AUC), using stepwise multiple regression analysis to select the top ranked n-1 biomarkers, and then combining the selected biomarkers using a linear discriminant function. A detailed description of the algorithm and its implementation in Stata 7.0 statistical package (Stata Corp, College Station, Texas) is provided in the Methods section and in Section 1 of the Additional File (see additional file 1). To assess the validity of our proposed algorithm, we used five datasets with 2 diagnostic classes each – four real datasets [17-20] (abbreviated as OvCa, LuMe, LLML and BrCa and described in Table 1) and a synthetically generated dataset (abbreviated as Syn1) comprising 50 samples of each diagnostic class and 1000 genes (described in the Methods section below).

Results from step 1 of the proposed algorithm

In the context of microarray experiments, the Zipf’s law suggests that there will be only few genes with very highly differential expression levels [21-24]. Analogous to this interpretation of the Zipf’s law, in our situation, we expected a small subset of biomarkers to be very highly discriminatory for diagnostic classification. Fig 2 shows that this indeed was the case. The proportion of biomarkers with performance index exceeding 0.4 (which corresponds to an AUC more than 0.9 or less than 0.1) was 0.31%, 2.36%, 1.25%, 0.03% and 11.1% in the OvCa, LuMe, LLML, BrCa and Syn1 datasets, respectively. This observation indicated that a combination of only few biomarkers is likely to be diagnostically sufficient.

Further, the OvCa dataset (as available from the source) was already normalized while the other three datasets used raw expression level values. As can be expected from the non-parametric nature of the area under the ROC curve statistic, this preprocessing (or the lack of it) of the data did not alter the diagnostic performance across the datasets. To explore this formally, we generated a synthetic dataset (Syn2) with 100 biomarkers and 100 subjects using raw as well as normalized expression values. The area under the ROC curve for the biomarkers – whether raw or normalized – was comparable (see Section 2 of additional file 1).

Results from step 2 of the proposed algorithm

As there were 132, 32, 38 and 43 subjects (Table 1) in the training subsets of the OvCa, LuMe, LLML and BrCa datasets, respectively, we chose 131, 31, 37 and 42 biomarkers in the corresponding full models in these datasets. We observed that the number of biomarkers that were retained in the final model in stepwise multiple linear regression analyses was strikingly low. For example, in the OvCa dataset 18 (of 131), in the LuMe dataset 5 (of 31), in the LLML dataset 3 (of 37) and in the BrCa dataset 5 (of 42) biomarkers were retained in the final model. In spite of these small number of biomarkers, the regression
The statistical algorithm used in the present study. Numbers correspond to the steps described in the text. Steps 1–3 were used on a training subset. The training subset was randomly chosen for the OvCa dataset while for the other two datasets, the training sets used by primary authors were used. Validation was done separately in the training and test subset within each dataset.

Table 1: The publicly available datasets used in the current study

| Characteristic       | Dataset #1 | Dataset #2 | Dataset #3 | Dataset #4 |
|----------------------|------------|------------|------------|------------|
| Authors              | Petricoin et al, 2002 [19] | Gordon et al, 2002 [18] | Golub et al, 1999 [17] | van't Veer et al 2002 [20] |
| Dataset alias        | OvCa       | LuMe       | LLML       | BrCa       |
| Biomarker            | Proteomic mass spectra | Gene expression | Gene expression | Gene expression |
| # Biomarkers         | 15,154     | 12,533     | 7,129      | 24,481     |
| Diagnostic classes   | Ovarian cancer | Normal    | Lung adeno-carcinoma | Mesothelioma | Acute lymphocytic leukemia | Acute myeloid leukemia | Metastasis within 5 years | Metastasis after 5 years |
| N (Total)            | 162        | 91         | 150        | 31         | 46         | 26         | 34         | 44         |
| N (Training)         | 83         | 49         | 16         | 16         | 27         | 11         | 17         | 26         |
| N (Test set)         | 79         | 42         | 134        | 15         | 19         | 15         | 17         | 18         |
The performance index ($P_i$) derived from the area under the ROC curve of the biomarkers within each dataset. The curves demonstrate that the diagnostic performance of the biomarkers follows the Zipf’s law. The colors for the four datasets are used consistently in Figure 3 and Supplementary Figures 1 and 2 (see additional file 1).

Results from step 3 of the proposed algorithm

Table 2 summarizes the results of the linear discriminant analyses. The discriminant scores for each dataset were obtained from the respective training subsets. It was observed that the discriminant score was clearly differentially clustered in the two diagnostic classes in each dataset (Fig. 3A to 3D) and that there was an extremely low or absent misclassification in the training set. The discriminant model fits as indicated by the model $R^2$, Mahalanobis $D^2$, $\chi^2$, canonical correlation coefficient, eigenvalues and Wilk’s $\lambda$ (Table 2) demonstrated that the model was highly suited for all the datasets used in this study. Within the training sets the discriminant rule correctly classified 100% of the subjects in all the training subsets of all the datasets.

Validation of the proposed algorithm

Next, we validated the diagnostic performance of the diagnostic rule in the three steps. First, an examination of the distribution of the discriminant score (insets to Fig 3E to 3H) revealed a markedly bimodal disposition in all the datasets suggesting the likelihood of an efficacious classification.

Second, we generated receiver operating characteristic (ROC) curves using the discriminant score as a predictor of the diagnostic class in the training subset as well as the test subset within each dataset. We observed that the Wilcoxon estimates AUC were high and comparably similar across the training- and test- sets within each of the three datasets (Fig 3E to 3H). Therefore, we estimated the overall prediction accuracy of the discriminant score for each dataset by combining the training- and test-subsets (Fig 3E to 3H).

The AUC for the discriminant score in the training and test sets combined were 100% (95% confidence interval not estimable) for the OvCa dataset, 99.9% (95% confidence interval 99.7%–100%) for the LuMe dataset, 96.7% (95% confidence interval 91.3% – 100%) for the LLML dataset and 94.3% (95 confidence interval 89.3% – 99.5%) for the BrCa dataset. The use of the AUC is only appropriate for this study because the high values of AUC indicate very high partial AUCs related to small false positives, which are required for a study of early detection of cancer. We have further addressed the issue of using AUC in the Discussion section. From these ROC curves we also observed that the cut-off points that maximized the discriminatory performance were -1.09 for the OvCa dataset, 0.43 for the LuMe dataset, -0.26 for the LLML dataset and 0.22 for the BrCa dataset corroborating the general assumption that positive and negative discriminant scores will indicate the two diagnostic classes. At these best cut-off points, we estimated the sensitivity and specificity of the discriminant score, the estimates for sensitivity and specificity were 100% and 100% for the OvCa dataset, 100% and 97% for the LuMe dataset, 98% and 92% for the LLML dataset, and 91% and 91% for the BrCa dataset, respectively.

Third, we scrutinized the list of biomarkers retained in the final model of the synthetically designed dataset (Syn1) of gene expression profile of 1000 hypothetical genes across 2 diagnostic classes in 100 subjects. In truth, the synthetic dataset contained 240 genes that were differentially expressed across the diagnostic classes. For details of the correlation among genes see Section 4 of the additional file 1. We observed that all the 22 genes retained in the final model (see Section 2e in the additional file 1) were included in the list of the known list of differentially expressed genes in this dataset thereby indicating that the algorithm did not falsely discover a differential expression of any gene in this dataset.

Comparison of the proposed algorithm with other methods

Our algorithm needs a single pass through the dataset for estimating the area under ROC curve for each biomarker and is, therefore, computationally less intense than other data mining techniques used in similar situations e.g. principal components analyses [25,26], singular value decomposition (SVD) [27,28], genetic algorithms (GA) [19], k-nearest neighborhood (kNN) [29,30], support vec-
Our suggested approach can directly estimate the local false discovery rate (FDR) which gives the probability that a biomarker identified to be associated with disease is in fact falsely identified [44]. Since the true association of a biomarker with the disease remains unknown, various methods exist that can be drawn for multiple category outcomes and the multidimensional ROC surface as a non-parametric measure of the diagnostic performance of each biomarker. A comparison of the results of these techniques with the results from our analyses in the real datasets used in this study (Table 3) demonstrates that the diagnostic accuracy of the proposed algorithm is comparable to or higher than that of the presently available analytical options. Also, in theSyn1 dataset we compared the classification performance of several currently used methods of classification with that of our proposed algorithm (Table 4) and observed a clear advantage of our algorithm – a parsimonious choice of the number of biomarkers without loss of diagnostic performance.

### Discussion

Our proposed statistical algorithm highly accurately classified subjects in all the datasets used in this study. The algorithm is simple, uses statistical techniques that are established in biostatistical literature and can be implemented by most statistical software packages. The choice between parametric versus non-parametric methods for analysis of microarray data has been a matter of intense debate [42]. It is possible that the high diagnostic accuracy achieved by our algorithm may be due to a combination of non-parametric and parametric methods. The suggested approach can be discounted on the basis of the fact that it differs from a more conventional approach of using Student’s t test only with regards to the use of area under the ROC curve. It is recognized that the area under the ROC curve follows a Mann-Whitney distribution [43]. Therefore, the first step in the suggested approach can be viewed narrowly as just a non-parametric alternative to the conventional approach.

However, in addition to its advantages mentioned earlier, the proposed algorithm offers one more subtle improvement. Since the true association of a biomarker with the disease remains unknown, various methods exist that indirectly estimate the local false discovery rate (FDR) which gives the probability that a biomarker identified to be associated with disease is in fact falsely identified [44]. Our suggested approach can directly estimate the local FDR (which in the lexicon of diagnostic test performance evaluation can be equated to the inverse of the positive predictive value) of a biomarker by varying the cut-off value for expression level over the observed range of values. This approach also does not presuppose a predefined single estimate of the local FDR. Indeed, the FDR can be allowed to vary based on the definition of expression level used for diagnostic classification. In spite of all these advantages, however, several caveats need to be mentioned before generalizing the results of the present study.

#### Study limitation 1: the choice of AUC for ranking biomarkers

The first step of our proposed algorithm makes use of ROC curves and therefore places some restrictions on the generalization of the approach to various situations. The real datasets that we used for validation in our study had diverse aims. For instance, the OvCa dataset was primarily designed for early detection of cancer, the LuMe and LLML datasets have therapeutic implications while the BrCa dataset has a prognostic significance. In the case of early detection of cancer, the emphasis is really on reducing the false positivity rate and, therefore, the area under the entire ROC curve may not be as useful [45]. However, in the analyses conducted in the present study our focus was on discriminating between two classes and all the datasets were used as examples of two class biomarker datasets. Fortuitously, in the OvCa dataset we found a perfect discrimination including the leftward of the ROC curve where the specificity was high.

#### Study limitation 2: the proposed algorithm is suitable for two classes only

First, our analysis demonstrates the use of the algorithm only in the situation of dichotomous classification. Theoretically, the technique can be extended to diagnostic outcomes with multiple classes. For example, ROC curves can be drawn for multiple category outcomes and the multi-class counterpart of the discriminant function analysis is available [46-51]. In that case, in the first step of our algorithm one would need to estimate the volume under the multidimensional ROC surface as a non-parametric measure of the diagnostic performance of each biomarker. A

Table 2: Summary of the discriminant model performance in the training subsets of the datasets used in the present study

| Statistic           | OvCa (n = 132) | LuMe (n = 32) | LLML (n = 38) | BrCa (n = 43) |
|---------------------|----------------|---------------|---------------|---------------|
| Model R²            | 0.9680         | 0.9618        | 0.9170        | 0.7436        |
| Wilk’s λ            | 0.0320         | 0.0382        | 0.0830        | 0.2564        |
| Mahalanobis D²      | 127.69         | 94.38         | 50.91         | 11.57         |
| χ²                  | 416.54         | 89.77         | 85.88         | 52.40         |
| Canonical correlation| 0.9839         | 0.9807        | 0.9576        | 0.8623        |
| Eigenvalue          | 30.26          | 25.17         | 11.05         | 2.90          |
Figure 3
The diagnostic performance of the proposed statistical algorithm. (A-D) The probability of the predicted diagnostic class in the training set of each dataset studied. Gradient background indicates a continually increasing or decreasing likelihood of the diagnostic classes. The abscissa indicates the discriminant score generated using the proposed algorithm. (E-H) Evaluation of the diagnostic performance of the proposed algorithm. The plots are ROC curves for the entire dataset (that is training and test sets combined) since the diagnostic performance of the discriminant score was consistently high in the training and test subsets when assessed separately. Area under the ROC curve (AUC) was non-parametrically estimated using the Wilcoxon method. Insets show the strikingly bimodal distribution of the discriminant scores in the entire (that is training and test subsets combined) datasets. SE, standard error.
potential difficulty can arise in the coding scheme to be used for the outcome variable for multiple linear regression analysis to be conducted in the second step of the algorithm. The coding scheme needs to be compatible with the assumption of linearity implicit in the regression analysis. As this compatibility is unlikely to be known a priori, we suggest that the numerical codes for the diagnostic classes be permuted and the regression be used for each permutation. One can, then, choose the regression that gives the best fit. Finally, one can use the multiclass discriminant function analysis on the chosen subset of biomarkers. In the present study, we did not conduct these analyses because Stata modules for estimating volume under surface and for multi-class discriminant analyses are not currently available.

Study limitation 3: the proposed algorithm cannot identify all the differentially expressed biomarkers

The algorithm is designed to make use of the diagnostic performance of a biomarker battery – it is not designed to identify all the biomarkers that are differentially expressed across the diagnostic classes. Consequently, exclusion of a biomarker from those retained in the analysis will not equate to a non-association of that biomarker with the disease state or process. For example, in the Syn1 dataset the algorithm chose only 22 of the actually 240 differentially expressed gene. Also, of the 18 biomarkers in the OvCa dataset that Zhu et al [41] had previously identified, only two were included in our list of 18 independent biomarkers. It has already been pointed out by Baggerly et al [52] and Sorace and Zhan [53] that the reproducibility of different methods in terms of the identified set of biomarkers using the same biomarker dataset is low. Ran- sohoff argues [54,55] that chance and bias are two major threats to the validity of inferences in studies attempting to associate molecular markers to disease status. For instance, the set of biomarkers identified to be significant may simply be a result of the way the training set was sampled from the full dataset. Indeed, Michiels et al [56,57] have demonstrated that the results obtained in the microarray experiments can be extremely sensitive to the sample size and procedure of selection of the training set. Notably, the training set used by Zhu et al [41] was not the same as the one we used in our analysis.

Study limitation 4: the choice of retention criterion for stepwise regression

The number of biomarkers finally retained in the stepwise regression analyses, will depend on the criterion used for retention (see Fig A2 in the additional file 1). In stepwise

| Dataset | Method | Reference | # biomarkers used | Accuracy (%) |
|---------|--------|-----------|-------------------|--------------|
| OvCa    | Principal components | Lilien et al, 2003 [25] | 1000 | 89 |
|         | Wilcoxon test | Sorace et al, 2003 [33] | 100 | 95 |
|         | Logical analysis of data | Alexe et al, 2004 [35] | 100 | 97 |
|         | Statgram | Zhu et al, 2003 [41] | 100 | 98 |
|         | Genetic algorithm | Petricoin et al, 2002 [19] | 88 – 94 | 97 |
|         | Proposed algorithm | Present study | 97 |
| LuMe    | Gene expression ratios | Gordon et al, 2002 [18] | 99 |
|         | Proposed algorithm | Present study | 100 |
| LLML    | Self-organizing maps | Toronen et al, 1999 [40] | 90 |
|         | Neural networks | Bicciato et al, 2003 [38] | 97 |
|         | ICED | Bijiani et al, 2003 [65] | 98 |
|         | Support vector machines | Furey et al, 2000 [66] | 88 – 94 |
|         | Proposed algorithm | Present study | 97 |
| BrCa    | Correlation | van’t Veer et al [20] | 83 |
|         | Proposed algorithm | Present study | 94 |

Table 3: Comparison of the results of the proposed algorithm with other approaches reported previously using the same datasets

Table 4: Comparison of the results of the proposed algorithm with other approaches using a simulated dataset (Syn1) of 100 samples and 1000 genes

| Method | Software | Reference | # biomarkers used | Accuracy (%) |
|--------|----------|-----------|-------------------|--------------|
| KMC    | Cleaver 1.0 | [67] | 1000 | 89 |
| kNN    | GeneCluster 2.0 | [68] | 127 | 95 |
| WV     | GeneCluster 2.0 | [68] | 127 | 97 |
| SAM    | SAM for Excel | [69] | 203 | 100 |
| PAM    | PAM for Excel | [69] | 224 | 100 |
| SVM    | GEPAS | [70] | 250 | 100 |
| Proposed | Stata 7.0 | [71] | 22 | 100 |
regression models, it is customary to use a probability criterion of 0.2. If this criterion is used in the biomarker analysis, it is evident that more number of biomarkers will be retained in the final model at the cost of an increased complexity of the subsequent discriminant rule. Moreover, considering the high level of accuracy that we obtained even with a very few biomarkers using a retention criterion 20 times as stringent, shows that there is indeed a very small scope for improving the diagnostic performance by relaxing the retention criterion. Again, because the purpose of the analysis was to optimize the diagnostic performance of a subset of biomarkers, to maintain the parsimony of the final regression model, we used a retention criterion of 0.01.

**Study limitation 5: potential bias implicit within the proposed algorithm**

We also considered if the algorithm itself is biased in favor of detecting non-existing i.e. false associations of biomarkers with disease states. For this purpose, we generated additional 1000 synthetic datasets (Syn3 – Syn1002) with 100 subjects and 100 biomarkers. Within each of these datasets, each biomarker expression followed a standard normal distribution N(0,1) and was thus non-differentially distributed across diagnostic classes. We then conducted the analyses using the proposed algorithm in each of the 1000 datasets and observed that in 92.8% of these samples the algorithm did not (as expected) find an association between any biomarker and the disease state. In the remaining 72 samples, the algorithm found association of one (67 samples) or two (5 samples) biomarkers with the disease. However, the R² values indicating the fit of the discriminant function model ranged from 0.0192 – 0.1574 (see Fig A3 in the additional file 1) suggesting that the model fits in these situations of non-existing associations were poor. If one compares these R² values with those reported in Table 2, it is clear that the algorithm did not detect false associations.

**Issues regarding inferences about validity**

To this end, we conducted a further series of analyses to ensure that the diagnostic accuracy of the proposed algorithm was not merely a result of chance or bias. (i) In the OvCa dataset, we generated 100 random training sets of varying sizes and within each of these training sets we estimated the AUC for each of the 15,154 markers (for details, see Fig A4 in the additional file 1). We then assessed the consistency of the AUC estimates in two ways: first, we conducted a factor analysis on the AUC estimates across all samples to assess whether the different training sets map onto a single domain versus multiple domains. We observed that training sets of sizes exceeding 100 were characteristically very similar to each other and consistently identified the same biomarkers. Second, we estimated the Spearman correlation coefficients between each of the random training sets and the training set that we used for the OvCa dataset. Predictably, we again observed that training sets exceeding sizes of 100 were very highly correlated with the training set that we used in this study. Since our training subset comprised of 132 subjects in the OvCa dataset, we believe that our results are unlikely to have been influenced by chance. (ii) We obtained bootstrap estimates of the AUC for all the biomarkers selected in the final model in 500 replicate samples (See Fig A4 in the additional file 1) for all the datasets. We observed that the estimate of AUC that we obtained in the chosen training set was always very close to the mean AUC obtained from 500 replicates even after correcting for sampling bias (see Fig A4C in the additional file 1). Thus, we believe that our results are robust and faithfully reflect true associations between biomarkers and disease status. (iii) Another important threat to validity that we considered was bias. Ransohoff [54] and Baggerly et al [52] also state that if bias in selecting the subjects in the main dataset is hard-wired into the study then demonstration of reproducibility will not be able to address this issue. Therefore, we conducted all our analyses across four different datasets of totally different characteristics. The fact that the proposed algorithm performed very well in all the datasets pointed towards the possibility that it is relatively insensitive to the element of bias specific to each of the chosen datasets. However, it is also possible that all the chosen datasets had negligible bias and therefore our results showed a consistently high performance of the proposed algorithm.

**Conclusion**

Within the constraints imposed by the caveats mentioned earlier, our analytical approach demonstrates a technique to translate molecular biomarker data into clinically meaningful and diagnostically useful information. Conceptually and in a broader context, the actual use of the biomarker batteries for detection of the disease status will depend on a conflation of three requisites – existence and severity of the disease under investigation; presence of sensitive and specific biomarkers and the choice of proper statistical analytical methods to ferret out the true relationships between disease and biomarkers. Using real and simulated datasets, in the present study we addressed the last two aspects only. In spite of the high discriminatory performance of the proposed statistical algorithm in the analytical situations considered, caution will be required before recommending molecular biomarkers as diagnostic tests against cancer as the existence and severity of cancer can substantially limit the generalizability of the results. Nevertheless, early and reliable diagnosis is the cornerstone of management of chronic diseases. In that vein and towards that goal, the proposed approach provides a simple, novel and accurate step.
Methods

The algorithm

Contingent upon the assumption that each biomarker can be considered as a diagnostic test, we designed a three-step procedure (Fig. 1) to arrive at an optimum combination of the biomarkers that will have a high degree of diagnostic accuracy. A theoretical basis for this improved diagnostic accuracy is that our proposed algorithm identifies a set of independent biomarkers that predict the disease class, and since each member of this set is ensured to be a good predictor of the disease status, a combination of these independent biomarkers will lead to an improved diagnostic accuracy. Following account describe the three steps in our proposed algorithm.

Step 1: quantification of diagnostic performance of biomarkers

In the first step, we estimate the diagnostic accuracy of each biomarker by plotting a ROC curve and estimating the area (A) under the ROC curve. The area under an ROC curve captures the overall diagnostic accuracy of the test. In our proposed algorithm, a non-parametric estimate of the area using trapezoidal rule is obtained in this step. Since, the area under an ROC curve is constrained within the interval (0, 1) and since an area of 0.5 represents maximum diagnostic uncertainty [58], we define a diagnostic performance index of the ith biomarker as \( P_i = |A_i - 0.5| \) where \( A_i \) is the estimated area under the ROC curve based on the expression pattern of the ith biomarker. This transformation of the area under ROC curve permits consideration of a bi-directional association of the biomarkers with the disease states such that either over- or under-expression of a particular biomarker can characterize the disease. Thus, the biomarkers can be ranked from highest to lowest values of \( P_i \) (for which the theoretical bounds are 0 and 0.5) with high values indicating diagnostically informative biomarkers and low values suggesting a low discriminatory performance of the biomarkers. However, since the diagnostic performance of one biomarker may be correlated with that of others, choosing the biomarkers with highest \( P_i \) values may not ensure independent and additive contribution of the biomarkers.

Step 2: optimizing the number of biomarkers

Therefore, the second step needs to be undertaken to optimize the set of biomarkers with high and independent diagnostic information content in a multivariate setting. Three critical issues need to be considered in this step: choosing an appropriate statistical method for multivariate analysis, choosing the number of diagnostically informative biomarkers to be entered into the multivariate model and using an appropriate method to optimize the number of finally selected biomarkers. With regard to choosing the statistical method, several choices present themselves. An obvious choice is to use the available methods to combine multiple diagnostic tests [16]. However, because one would have only achieved, in step 1, a ranked list of biomarkers; there remains the circular problem of trying to predefine the number of biomarkers to be combined. Another option is to use multivariate regression analyses. As the outcome variable is – by definition – dichotomous, the likely choices can be methods like logistic regression or probit regression. However, since the predictor biomarkers will be selected on the basis of high diagnostic performance \( (P_i) \) it is extremely likely that these will be highly discriminant across the outcome states. Consequently, the regression coefficients in a logistic regression model may not be estimable (because of, for instance, an infinite odds ratio) and these highly informative biomarkers are likely to be automatically dropped from the model by statistical software packages. Therefore, we suggest the use of multivariate linear regression with the outcome variable being the codes for the dichotomous disease states (0/1).

The second issue relates to the number of biomarkers to be included in the multivariate linear regression model. This is not difficult in the context of a multivariate regression model because for a regression model to be identifiable the number of covariates must be less than the number of observations. Thus, the number of most discriminant biomarkers that can be included in this model must be less than the number of subjects included in the analysis. Finally, the third critical issue relates to the method of optimizing the number of biomarkers included in the multivariate analysis. We suggest the approach of a stepwise regression using backward elimination procedure. Considering the fact that the purpose of this step is to optimize the cardinality of the subset of diagnostically useful biomarkers, we suggest the use of a strict retention criterion, that is, the maximum significance value needed to retain a biomarker in the multivariate model. It is evident that the more rigid this criterion, the lesser the number of biomarkers that will be selected in the final model. In our analyses we used a retention criterion of 0.01.

Step 3: generating a diagnostic classification based on the optimized subset of biomarkers

Linear discriminant function model is an extension of the linear regression model but can also be used in place of logistic regression [59,60]. Therefore, we suggest the use of a linear discriminant score using the optimized subset of biomarkers identified in the previous step. The discriminant model fit can be assessed by model \( R^2 \) and its complement – Wilk’s \( \lambda \) (which varies between 0 and 1 with a smaller value indicating a better fit). If the model fit is good, then for a given subject a discriminant score can be generated using the unstandardized discriminant regression coefficients and the expression levels of chosen biomarkers. The discriminant function analysis reports
the centroids of the discriminant scores for subjects belonging to different diseases states. These can be used to predict the disease status in a given subject. Generally, positive and negative values of the diagnostic score will indicate two different disease states depending on the discriminatory performance of the score. Thus, while use of discriminant function analysis itself is not new to the field of microarray data analysis [61-63], we here propose a novel way to choose a diagnostically discriminant subset of biomarkers by using the results of a stepwise regression analysis procedure.

Validation of the proposed algorithm
To validate the proposed analytical approach, we used four publicly available datasets (Table 1). Before applying the algorithm to derive a discriminatory rule, we split each original dataset into a training set (to derive the rule) and a validation set (to test whether the rule discriminates between the same diagnostic classes in an independent group of subjects). This split was done once, before any analysis, and the resulting validation set was used only once for the primary analysis. We conducted the validation of this rule in three steps. First, we applied the discriminant rule to the independent test subset. Additionally, we also reported the validation performance of the discriminant score in the training as well as entire dataset. The diagnostic performance of the discriminant score was assessed by estimating sensitivity, specificity and diagnostic accuracy by plotting the ROC curves. Second, we compared the results of our proposed approach to those reported for other available methods of classification using the same four real datasets that we included in the present study. Third, we created a synthetically designed dataset with known set of differentially expressed genes and assessed whether the biomarkers retained in the final model of the proposed algorithm are a subset of the known differentially expressed genes in the synthetic dataset. Also, in this synthetic dataset, we compared the diagnostic performance of the proposed algorithm with that of other methods used for this purpose.

Datasets
For validation of the proposed algorithm, we used four real datasets and a synthetically designed dataset. The four real datasets (Table 1) were: serum proteomic profile of ovarian cancer subjects and controls (referred here as OvCa data) [19], gene expression data of subjects with adenocarcinoma of lung compared to subjects with mesothelioma (LuMe dataset) [18] and gene expression pattern of subjects with acute lymphocytic leukemia compared with that of subjects with acute myeloid leukemia (LLML dataset) [17] and breast cancer subjects followed prospectively for development of metastasis within or after 5 years of follow-up (BrCa dataset) [20]. The synthetically designed dataset (Syn1) was generated using the SIMAGE software package [64]. This dataset contained expression values for 1000 genes for two diagnostic classes with 50 subjects each. The detailed specifications and input parameters used to generate this dataset are provided in Section 4 in the additional file (see additional file 1). Apart from these five datasets we used a synthetic dataset (Syn2) to examine the influence of data preprocessing on the estimates of AUC (see Section 2 of the additional file 1) and 1000 datasets (Syn3 – Syn1002, see Fig A3 in the additional file 1) to assess the likelihood of false discovery in the use of the proposed algorithm. All the statistical analyses were conducted using Stata 7.0 (College Station, Texas) software package.

Competing interests
The author(s) declare that they have no competing interests.

Authors’ contributions
MRM and HK conceptualized the study, conducted data analysis and wrote initial and revised drafts of the manuscript. TPT wrote parts of the manuscript and critically reviewed all the drafts. MYK, MAA, YVK and APA critically reviewed the manuscript. All authors read and approved the final manuscript.

Additional material

Additional File 1
This file contains 4 sections and 4 figures. The first section provides a detailed account of the implementation of the proposed algorithm using Stata 7.0 statistical package. Section 2 demonstrates that the AUC estimates obtained in the first step of the proposed algorithm are not influenced by preprocessing of the data. Section 3 provides detailed output from Stata to support the results described in the text while Section 4 details the input parameters used to generate the Syn1 synthetic dataset. The file also provides ROC curves for individual biomarkers (Fig A1), influence of the retention criterion on the diagnostic performance of the algorithm (Fig A2), distribution of R2 estimates in 1000 synthetic datasets (Fig A3) and influence of the procedure to select a training set on the diagnostic performance of the algorithm (Fig A4).

Click here for file
[http://www.biomedcentral.com/content/supplementary/1471-2105-7-442-S1.doc]

Acknowledgements
We gratefully acknowledge the critical thinker and reviewer who wishes to remain anonymous but because of whom the manuscript greatly improved at the pre-review stage. We also gratefully acknowledge the reviewers of our manuscript for insightful and thorough reviews which further enhanced the manuscript. Lastly, we acknowledge the spirit of science with which the original datasets have been shared for public use by the primary authors.
References

1. Armstrong NJ, van de Wiel MA: Microarray data analysis: from hypotheses to conclusions using gene expression data. Cell Oncol 2004, 26(5-6):279-290.

2. Gaasterland T, Bekiranov S: Making the most of microarray data. Nat Genet 2000, 24(3):204-206.

3. Li L, Tang H, Wu Z, Gong J, Grudii M, Zou J, Tockman M, Clark RA: Data mining techniques for cancer detection using serum proteomic profiling. Afr J Intel Med 2004, 31(2):71-83.

4. Man MS, Dyka G, Johnson K, Liao B: Evaluating methods for classifying expression data. J Bioph Stat 2004, 14(4):1065-1084.

5. Brentani RR, Carraro DM, Verjovski-Almeida S, Reis EM, Neves EJ, de Souza SJ, Carvalho AF, Brentani H, Reis LF: Gene expression analysis and cancer research: methods and applications. Crit Rev Oncol Hematol 2005, 54(2):95-105.

6. Draghici S: Statistical intelligence: effective analysis of high-density microarray data. Drug Discov Today 2002, 7(11 Suppl):555-63.

7. Betrin CB, Bhatra RM: Microarray technology - enhanced versatility, persistent challenge. Curr Opin Biotechnoll 2000, 11(1):36-41.

8. Hatfield GW, Hung SP, Baldi P: Differential analysis of DNA microarray gene expression data. Mal Microbiol 2003, 47(4):871-877.

9. Ntzani EE, Ioannidis JP: Predictive ability of DNA microarrays for cancer outcomes and correlates: an empirical assessment. Lancet 2003, 362(9394):1439-1444.

10. Tabd Z: Statistical analysis of oligonucleotide microarray data. C R Biol 2004, 327(3):175-180.

11. Mendez MA, Hodor C, Vulpe C, Gonzalez M, Cambiazo V: Discriminant analysis to evaluate clustering of gene expression data. FEBS Lett 2002, 522(1-3):24-28.

12. Soukup M, Lee JY: Developing optimal prediction models for cancer classification using gene expression data. J Bioinform Comput Biol 2004, 1(4):681-694.

13. Jung SH, Bang H, Young S: Sample size calculation for multiple testing in microarray data analysis. Biostatistics 2005, 6(4):531-537.

14. Baker SG: Identifying combinations of cancer markers for further study as triggers of early intervention. Bioinformatics 2000, 56(4):1082-1087.

15. Pepe MS, Longton G, Anderson GL, Schummer M: Selecting differentially expressed genes from microarray experiments. Biometrics 2003, 59(1):133-142.

16. Xiong C, McKeel DWJ, Miller JP, Morris JC: Identifying combinations of cancer markers for further study as triggers of early intervention. J Magn Reson 2004, 205(4):1638-1643.

17. Golub TR, Slonim DK, Tamayo P, Huard C, Gaasenbeek M, Mesirov JP, Coller H, Loh ML, Downing JR, Caligiuri MA, Bloomfield CD, Lander ES: Molecular classification of cancer: class discovery and class prediction by gene expression monitoring. Science 1999, 286(5439):539-543.

18. Gordon GJ, Jensen RV, Hsiao LS, Gullans SR, Blumenstock JE, Ramaswamy S, Richards WG, Sugarbaker DJ, Burtin R: Translation of microarray data into clinically relevant cancer diagnostic tests using gene expression ratios in lung cancer and mesothelioma. Cancer Res 2002, 62(17):4963-4967.

19. Petsch M, Ardekani AM, Hix BA, Levine PJ, Fusaro VA, Steinberg SM, Mills GB, Cussenot C, Fishman DA, Kohn EC, Liotta LA: Use of proteomic patterns in serum to identify ovarian cancer. Lancet 2002, 359(9306):572-577.

20. van ’t Veer LJ, Dai H, van de Vijver MJ, He YD, Hart AA, Mao M, Peterse HL, van der Kooy K, Marton MJ, Witteveen AT, Schreiber GJ, Kerkvloem RM, Roberts C, Linley PS, Bernards R, Friend SH: Gene expression profiling predicts clinical outcome of breast cancer. Nature 2002, 415(6871):530-536.

21. Furlanello C, Serafini M, Merler S, Jurman G: Entropy-based gene ranking without selection bias for the predictive classification of microarray data. BMC Bioinformatics 2003, 4(1):54.

22. Hoyle DC, Rattray M, Jupp R, Brass A: Making sense of microarray data distributions. Bioinformatics 2002, 18(4):576-584.

23. Li WY, Yang Y: Zipf’s law in importance of genes for cancer classification using microarray data. J Theor Biol 2002, 219(4):539-551.

24. Lu T, Costello CM, Croucher PJ, Hasler R, Deuschl G, Schreiber S: Can Zipf’s law be adapted to normalize microarrays? BMC Bioinformatics 2005, 16(1):7.

25. Lillen RH, Farid H, Donald BR: Probabilistic disease classification of expression-dependent proteomic data from mass spectrometry of human serum. J Comput Biol 2003, 10(6):925-946.

26. Sharrar AA, Dudekula DB, Ko MS: A web-based tool for principal component analysis and significance analysis of microarray data. Bioinformatics 2005.

27. Ghosh D: Singular value decomposition regression models for classification of tumors from microarray experiments. Pac Symp Biocomput 2002:18-29.

28. Wall ME, Dyck PA, Breetzke TS: SVDMAN--singular value decomposition analysis of microarray data. Bioinformatics 2001, 17(6):566-568.

29. Li L, Lumbach DM, Terry P, Taylor J: Application of the GA/KNN method to SELDI proteomics data. Bioinformatics 2004, 20(18):1638-1640.

30. Pan F, Wang B, Hu X, Perrizo W: Comprehensive vertical sample-based KNN/L SVM classification for gene expression analysis. J Biomed Inform 2004, 37(4):240-248.

31. Kohlinna M, Schloch C, Schnittger S, Dugas M, Hiddemann W, Kern W: Haferlach T, Pedir A: Identification of phosphatidylinositol 3-kinase pathway activation in lymphoblastic leukemia (ALL): gene expression signatures classify an independent cohort of adult ALL patients. Leukemia 2004, 18(1):63-71.

32. Lee Y, Lee CK: Classification of multiple cancer types by multiclass support vector machines using gene expression data. Bioinformatics 2005, 21(19):3326-3335.

33. Shannon W, Culverhouse R, Levy S: A comprehensive evaluation of multiclassification methods for microarray gene expression cancer diagnosis. Bioinformatics 2005, 21(5):631-643.

34. Alexe G, Alexe S, Liotta LA, Petricoin E, Reiss M, Hammer PL: Ovarian cancer detection by logical analysis of proteomic data. Proteomics 2004, 4(3):766-779.

35. Ando T, Suguro M, Hanai T, Kobayashi T, Honda H, Seto M: Fuzzy neural network applied to gene expression profiling for predicting the prognosis of diffuse large B-cell lymphoma. Jpn J Cancer Res 2002, 93(11):1207-1212.

36. Berriz DP, Downes CS, Dubitzky W: Multiclass cancer classification using gene expression profiling and probabilistic neural networks. Pac Symp Biocomput 2003:5-16.

37. Bicciato S, Pandini M, Didone G, Di Bello C: Pattern identification and classification in gene expression data using an autoassociative neural network model. Biotechnol Bioeng 2003, 81(5):594-606.

38. Linder R, Dew D, Sudhoff H, Theegarten D, Remberger K, Poppl SJ, Wagner M: The subsequent artificial neural network (SANN) approach might bring more classificatory power to ANN-based DNA microarray analyses. Bioinformatics 2004, 20(18):3544-3552.

39. Teronon P, Kolehmainen M, Wong G, Castren E: Analysis of gene expression data using self-organizing maps. FEBS Lett 1999, 451(2):142-146.

40. Zhu W, Wang X, Ma Y, Rao M, Glimm J, Kovach JS: Detection of cancer-specific markers amid massive mass spectral data. Proc Natl Acad Sci U S A 2003, 100(25):14666-14671.

41. Giles PJ, Kipling D: Normality of oligonucleotide microarray data and implications for parametric statistical analyses. Bioinformatics 2003, 19(17):2254-2262.

42. Faraggi D, Reiser B: Estimation of the area under the ROC curve. Stat Med 2002, 21(28):3093-3106.

43. Tsai CA, Chen JH: Significance analysis of ROC indices for comparing diagnostic markers: applications to gene microarray data. J Bioph Stat 2004, 14(4):985-1003.

44. Baker SG, Kramer BS, McIntosh M, Patterson BH, Shyr Y, Skates S: Evaluating markers for the early detection of cancer: overview of study designs and methods. Clin Trials 2006, 3(1):43-56.

45. Devos A, Lukas L, Suykens JA, Van Hamme L, Tate AR, Howe FA, Majos C, Moreno-Torres A, van der Graaf M, Arus C, Van Huffel S: Classification of brain tumours using short echo time 1H MR spectroscopy. J Magn Reson 2004, 170(1):164-175.
47. Dreiseitl S, Ohno-Machado L, Binder M: Comparing three-class diagnostic tests by three-way ROC analysis. Med Decis Making 2000, 20(3):323-331.
48. Kim TK, Kitterl J: Locally linear discriminant analysis for multimodally distributed classes for face recognition with a single model image. IEEE Trans Pattern Anal Mach Intell 2005, 27(3):318-327.
49. Lukas L, Devos A, Suykens JA, Vanhamme L, Howe FA, Majos C, Moreno-Torres A, Van der Graaf M, Tate AR, Arus C, Van Huffel S: Brain tumor classification based on long echo proton MRS signals. Artif Intell Med 2004, 31(1):73-89.
50. Nakas CT, Yannoutsos CT: Ordered multiple-class ROC analysis with continuous measurements. Stat Med 2004, 23(22):3437-3449.
51. Yang H, Carlin D: ROC surface: a generalization of ROC curve analysis. J Biopharm Stat 2000, 10(2):183-196.
52. Baggerly KA, Morris JS, Edmonson SR, Coombes KR: Signal in noise: evaluating reported reproducibility of serum proteomic tests for ovarian cancer. J Natl Cancer Inst 2005, 97(4):307-309.
53. Sorace JM, Zhan M: A data review and re-assessment of ovarian cancer serum proteomic profiling. BMC Bioinformatics 2003, 4(1):24.
54. Ransohoff DF: Bias as a threat to the validity of cancer molecular-marker research. Nat Rev Cancer 2005, 5(2):142-149.
55. Ransohoff DF: Lessons from controversy: ovarian cancer screening and serum proteomics. J Natl Cancer Inst 2005, 97(4):315-319.
56. Michiels S, Koscielny S, Hill C: Prediction of cancer outcome with microarrays. Lancet 2005, 365(9472):1684-1685.
57. Michiels S, Koscielny S, Hill C: Prediction of cancer outcome with microarrays: a multiple random validation strategy. Lancet 2005, 365(9458):488-492.
58. Hanley JA, McNeil BJ: The meaning and use of the area under a receiver operating characteristic (ROC) curve. Radiology 1982, 143(1):29-36.
59. Bock JR, Afifi AA: Estimation of probabilities using the logistic model in retrospective studies. Comput Biomed Res 1988, 21(5):449-470.
60. Nagino M, Nimura Y, Hayakawa N, Kima J, Kondo S, Sasaki R, Hamajima N: Logistic regression and discriminant analyses of hepatic failure after liver resection for carcinoma of the biliary tract. World J Surg 1993, 17(2):250-255.
61. Dabney AR: Classification of microarrays to nearest centroids. Bioinformatics 2005, 21(22):4148-4154.
62. Dudoit S, Fridlyand J, Speed TP: Comparison of discrimination methods for the classification of tumors using gene expression data. J Am Stat Assoc 2002, 97:77-87.
63. Lee JW: An extensive comparison of recent classification tools applied to microarray data. Comput Stat Data Anal 2005, 48:869-885.
64. Albers CJ, Jensen RC, Kok J, Kuipers OP, van Hium SA: SIMAGE: simulation of DNA-microarray gene expression data. BMC Bioinformatics 2006, 7:205.
65. Bijlani R, Cheng Y, Pearce DA, Brooks AI, Oghara M: Prediction of biologically significant components from microarray data: Independently Consistent Expression Discriminator (ICED). Bioinformatics 2003, 19(1):62-70.
66. Furey TS, Cristianini N, Duffy N, Bednarski DW, Schummer M, Huusler D: Support vector machine classification and validation of cancer tissue samples using microarray expression data. Bioinformatics 2000, 16(10):906-914.
67. Raychaudhury S, Sutphin PD, Stuart JM, Altman RB:. [http://classify.stanford.edu/]. Stanford
68. Broad Institute:. [http://www.broad.mit.edu/cancer/software/genecluster/gc2.html]. Cambridge
69. Tibshirani R, Hastie T, Narasimhan B, Chu G: Diagnosis of multiple cancer types by shrunken centroids of gene expression. Proc Natl Acad Sci U S A 2002, 99(10):6567-6572.
70. Vaquerizas JM, Conde L, Yankelevich P, Cabazon A, Miguez P, Diaz-Urarte R, Al-Shahrour F, Herrero J, Dopazo J: GEPAS, an experiment-oriented pipeline for the analysis of microarray gene expression data. Nucleic Acids Res 2005, 33(Web Server issue):W616-20.
71. Stata_Corp:. 7.0 [http://www.stata.com/]. College Station