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An experimental study of low-velocity impacts into granular material in reduced gravity

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ABSTRACT

In order to improve our understanding of landing on small bodies and of asteroid evolution, we use our novel drop tower facility to perform low-velocity (2–40 cm s⁻¹), shallow impact experiments of a 10 cm diameter aluminum sphere into quartz sand in low effective gravities (~0.2–1 m s⁻²). Using in situ accelerometers, we measure the acceleration profile during the impacts and determine the peak accelerations, collision durations and maximum penetration depth. We find that the penetration depth scales linearly with the collision velocity but is independent of the effective gravity for the experimental range tested, and that the collision duration is independent of both the effective gravity and the collision velocity. No rebounds are observed in any of the experiments. Our low-gravity experimental results indicate that the transition from the quasi-static regime to the inertial regime occurs for impact energies two orders of magnitude smaller than in similar impact experiments under terrestrial gravity. The lower energy regime change may be due to the increased hydrodynamic drag of the surface material in our experiments, but may also support the notion that the quasi-static regime reduces as the effective gravity becomes lower.

Key words: comets: general–minor planets, asteroids: general–planets and satellites: surfaces.

1 INTRODUCTION

Space missions (e.g. Veverka et al. 2000; Robinson et al. 2002; Sullivan et al. 2002; Fujiwara et al. 2006; Coradini et al. 2011; Jaumann et al. 2012) and thermal infrared observations (e.g. Campins et al. 2009; Gundlach & Blum 2013; Delbo et al. 2015) have revealed that asteroids are covered with substantial regolith (the loose unconsolidated material that comprises the upper portions of an asteroid; Robinson et al. 2002). Several current and future small body missions include lander components, e.g. MASCOT and the MINERVA rovers on-board Japan Aerospace Exploration Agency (JAXA)’s Hayabusa-2 mission (Tsuda et al. 2013), MASCOT-2 and possibly AGEX on-board European Space Agency (ESA)’s Asteroid Impact Mission (Ho et al. 2016; Karatekin et al. 2016; Michel et al. 2016). Given the small escape velocities of these missions’ targets, the landing velocities are likely to be small (10s of cm s⁻¹ or lower) in order to minimize the risk of rebounding into space. The understanding of low-velocity surface–lander interactions is, therefore, important for all missions with lander components and will influence the lander deployment strategy, the mission design and operations, and even the choice of payload for the future missions (e.g. Murdoch et al. 2016). The dynamics of low-velocity interactions with granular material in reduced gravity are also important for other missions, such as OSIRIS-REx (NASA), that will interact directly with the asteroid’s surface in order to retrieve a regolith sample (Lauretta & OSIRIS-Rex Team 2012).

In addition to being of high importance for future space missions, the physics of low-velocity collisions in low gravity also has consequences for our understanding of planetary accretion processes, planetary ring dynamics, cratering processes, asteroid geophysical evolution, and our interpretations of small body surfaces. For example, rubble-pile asteroids such as (25143) Itokawa are thought to be formed via a catastrophic disruption event and subsequent re-accumulation (e.g. Michel et al. 2001). The impact velocity during re-accumulation is limited by the escape velocity of the body.
(≈10 cm s\(^{-1}\) for Itokawa; Fujiwara et al. 2006) and, as such, the collisions involved are necessarily at low velocity. Experimental research can improve our understanding of the different processes that may arise during gravitational re-accumulation such as rebounding or burial of the impacting particle or boulder, regolith mixing or secondary crater formation (Nakamura et al. 2008).

Using the ISAE-SUPAERO drop tower (Sunday et al. 2016), we have performed a series of low-velocity collisions into granular material in reduced gravity. Reduced gravity is simulated by releasing a free-falling projectile into a surface container with a downward acceleration less than that of Earth's gravity. The acceleration of the surface is controlled through the use of an Atwood machine or a system of pulleys and counterweights. This system provides a means to reduce the effective surface acceleration of the granular material. Since both the surface and projectile are falling, the projectile requires some time to catch up with the surface before the collision begins. This extended free-fall period increases the experiment duration, making it easier to use accelerometers and high-speed cameras for data collection. The experiment is built into an existing 5.5 m drop tower frame (originally built for aircraft and material drop-tests; Israr et al. 2014) and has required the custom design of all components, including the projectile, surface sample container and release mechanism (Sunday et al. 2016). The design of our experiment accommodates effective accelerations of ≈0.1–1.0 m s\(^{-2}\). This is lower than in previous experiments (e.g. Goldman & Umbanhowar 2008; Alshuler et al. 2014), allowing us to come closer to the conditions found at the surface of asteroids.

Here we will first discuss previous work in the field of low-velocity granular collisions, before describing the experiment, the data collection and the data analysis. Finally, we present the results of our experimental trials and discuss the implications for small body missions and asteroid evolution.

2 LOW-VELOCITY GRANULAR IMPACTS
Granular materials exhibit several characteristics that make them interesting but equally very difficult to understand. Unlike solids, they can conform to the shape of the vessel containing them, thereby exhibiting fluid-like characteristics. On the other hand, they cannot be considered a fluid, as they can be heaped (Gudhe, Yalamanchili & Massoudi 1994). The micro-gravity environment at the surface of an asteroid, in combination with the granular surfaces, challenges existing theoretical models. In this paper, we focus specifically on low-velocity granular impacts; however, for a detailed discussion of granular materials in the context of small body science, including many other applications where understanding granular dynamics in low gravity is important, the reader is referred to Murdoch et al. (2015).

As mentioned above, low-velocity impacts into granular material are of interest for many aspects of planetary science (planetary accretion, planetary ring dynamics, cratering, asteroid re-accumulation, regolith mixing,...) and for current and future space missions that will interact with the surfaces of small bodies. However, the subject of granular impacts is also of great interest to the granular physics community and has been the focus of multiple studies. For example, as the resulting crater depth relates to the stopping force on the impactor, the maximum penetration depth in a granular impact can be used to probe granular mechanics. Uehara et al. (2003), Newhall & Durian (2003) and Ambroso et al. (2005) show experimentally that under terrestrial gravity, the final penetration depth (\(z\)) of a spherical or cylindrical projectile impacting a dry granular material (glass beads) is related to the drop height (\(H\)) as \(z \sim H^{1/3}\) (or to the collision velocity as \(z \sim V^{2/3}\)). Tsimring & Volfson (2005) found the same dependance using numerical simulations. The experiments of Goldman & Umbanhowar (2008) and de Bruyn & Walsh (2004), on the other hand, demonstrate a linear scaling of penetration depth with impact velocity (\(z \sim V\)) for impacts of spheres into glass beads. This linear scaling with impact velocity was also found in the numerical simulations of Pica Ciamarra et al. (2004). The different scaling relationships may arise due to different packing fractions of the granular materials (de Bruyn & Walsh 2004) or due to the differences between shallow and deep penetration experiments (Uehara et al. 2003; Walsh et al. 2003).

The collision time for a spherical impactor is found to be independent of the collision velocity at higher collision velocities (Pica Ciamarra et al. 2004; Goldman & Umbanhowar 2008), but for lower collision velocities (<1.5 m s\(^{-1}\)), the collision duration increases with decreasing collision velocity.

The determination of the drag force during penetration was the focus of the work by Nakamura et al. (2013), who attempt to better understand the penetration of particles into regolith during the gravitational re-accumulation process of an asteroid following a catastrophic disruption. To do this, they study the deceleration of spherical plastic projectiles as they impact glass beads at speeds of ≈70 m s\(^{-1}\). The experiments, performed under both terrestrial gravity and micro-gravity (using a parabolic flight), allowed estimates to be made of the penetration depth of an impactor on an asteroid surface.

With the aim of investigating planetesimal growth and planetary ring dynamics, Colwell & Taylor (1999) and Colwell (2003) studied micro-gravity collisions into granular surfaces over the course of two different payload experiments aboard the Space Transportation System (Space Shuttle). In the first set of experiments (Colwell & Taylor 1999), spherical Teflon projectiles of 0.96 and 1.92 cm diameter impacted into JSC-1 (a glass-rich basaltic ash similar to lunar mare regolith) at 10–100 cm s\(^{-1}\) in order to study both the coefficient of restitution and the ejecta velocities. They found that virtually no ejecta was produced in these collisions and the coefficients of restitution were very low (0.02–0.03). These experiments were later repeated with 2 cm diameter projectiles and less compacted targets of JSC-1 and quartz sand (Colwell 2003). Again, coefficients of restitution of 0.01–0.02 were observed for impacts in the 15–110 cm s\(^{-1}\) range but no rebound was observed for impacts at less than 12 cm s\(^{-1}\). This time, however, in the higher velocity impacts (>25 cm s\(^{-1}\)), some ejecta was observed from the loose quartz sand targets. The extension of this same experiment to even lower impact energies was achieved by Colwell et al. (2015) who completed a series of micro-gravity impact tests over three parabolic flights. These results showed an increase in the coefficient of restitution for marbles impacting JSC-1 at very low impact velocities (~5 cm s\(^{-1}\)). These Space Shuttle and parabolic flight experiments were very successful but the need for future experiments varying the impactor mass and impactor velocity was highlighted (Colwell & Taylor 1999; Colwell 2003).

Having accelerometers inside the projectiles allows for a better understanding of the impact dynamics. Such experiments were performed by Goldman & Umbanhowar (2008), both under terrestrial gravity and in reduced-gravity making use of an Atwood machine similar to the experiment described here. In their study, the acceleration of spherical and disc-shaped projectiles was measured during the impact into granular material (glass beads). They showed that the peak acceleration of a sphere during the impact scales with the
square of the impact velocity; however, this scaling does not hold for impact velocities $<1.5\, \text{m}\,\text{s}^{-1}$. Additionally, for spheres, the collision duration is found to be independent of the collision velocity at impact velocities $>1.5\, \text{m}\,\text{s}^{-1}$, but at lower impact velocities, the collision duration increases with decreasing impact velocity. The opposite effect is seen for an impacting disc, with the collision duration decreasing significantly at low impact velocities.

Altshuler et al. (2014) also use an Atwood machine to study impacts of spheres into polystyrene beads in varying gravity. They found that the maximum penetration depth of the projectile into the granular material was independent of the gravitational acceleration. Also, in addition to the finding of Goldman & Umbanhowar (2008) that the collision time increases with decreasing velocity for a spherical impactor, Altshuler et al. (2014) find that the collision duration also increases with decreasing gravity. It should be noted, however, that the extrapolation to very low gravity levels ($<0.4\, \text{m}\,\text{s}^{-2}$) was made using numerical simulation data and not experimental data.

These last two studies (Goldman & Umbanhowar 2008; Altshuler et al. 2014) have started to investigate the role of gravity during low-velocity granular impacts. However, the experiments have collision velocities of $\sim\text{40–70 cm}\,\text{s}^{-1}$ and gravity levels $>0.4\, \text{m}\,\text{s}^{-2}$. Here we use the ISAE-SUPAERO drop tower experiment (Sunday et al. 2016) in order to achieve lower and variable gravity levels, lower collision velocities and to increase the size of the experiment. The scale of our experiment allows us to use a larger projectile (10 cm; closer in size to an asteroid lander) that contains accelerometers in order to study in detail the impact dynamics during the low-velocity, low-gravity collisions. As a secondary data source, we also use a static rapid, high-resolution camera. Also, rather than using glass or polystyrene beads, we use quartz sand in our experiment in order to be more representative of the regolith found on small bodies.

### 3 EXPERIMENT DETAILS

The detailed experiment design is described in Sunday et al. (2016). Here, we just give a short overview of the key aspects. The acceleration of the surface is controlled through the use of an Atwood machine, or a system of pulleys and counterweights, which allows the surface container to have a constant downward acceleration less than that of gravity. If pulley friction and chord elasticity are neglected, then the controlled acceleration is simply a function of mass. The expression for the surface container’s acceleration ($a_s$) is derived by balancing the forces on the surface container and counterweights. This is given by equation (1), where $m_s$ is the mass of the surface container, $m_{cw}$ is the total combined mass of all counterweights and $g$ is the Earth’s gravitational acceleration.

$$a_s = g \left( \frac{m_s - m_{cw}}{m_s + m_{cw}} \right).$$

The effective gravity of the surface container ($g_{eff}$) is then the difference between the Earth’s gravitational acceleration and the acceleration of the surface container, i.e. $g_{eff} = g - a_s$.

The experiment is built into an existing 5.5 m drop tower frame and has required the custom design of all components, including the projectile, surface sample container and release mechanism. The counterweight holders alone weigh 400 g each. Then, mass can be added to the holders at 100 g increments in order to change the acceleration of the surface container. Fig. 1 shows the mounted pulley system, and the counterweight, and guide tube components of the assembly.

![Figure 1. Isometric line drawing of the experiment and surface container. Isometric line drawing of the (upper figure) drop tower structure and (lower figure) surface container sub-assembly. The experiment’s custom-designed subsystems include the surface container (outer dimensions: 62 cm long, 45 cm wide and 59 cm high), projectile (10 cm diameter), electromagnetic release mechanism, pulley and counterweight system, and deceleration material. The reference markings for image post-processing can also be seen on the surface container. Images from (Sunday et al. 2016).](image-url)
3.1 Sensors

3.1.1 Accelerometers

YEI 3-Space Sensors (YEI Technology 2013) are mounted to the projectile and surface container. These sensors are data-logging devices that contain an Attitude and Heading Reference System, an Inertial Measurement Unit, and a micro-SD card for on-board data storage. The YEI 3-Space Sensors were specifically selected because of their low mass, high sensitivity, and high shock resistance (see Table 1). These features allow the sensors to record the impact between the projectile and the sand with high precision and to survive the final shock at the end of the drop. Several data filtering options are available as part of the sensors. We use only the data logging capability with no automatic filtering giving the maximum sampling frequency possible of $\sim 1200$ Hz.

3.1.2 Cameras

A high-resolution camera (Ultima APX-RS Photron FASTCAM) is used with a Sigma 24–70 mm f/2.8 DG lens, to capture high-speed images (1000 frames per second) of the projectile–sand collision with a 1024 $\times$ 1024 pixel resolution. The camera was static and was placed at a distance of $\sim 2.7$ m from the front of the surface container and a focal length of 24 mm was used for the lens. This gives a pixel resolution of $\sim 5$ pixels per cm at the front panel of the surface container. In addition, a small, wide angle (175$^\circ$) camera (PNJ AEE MagiCam SD100) was fixed inside the surface container to give an in situ view of the experiment. This camera has a pixel resolution of 1920 $\times$ 1080 and captures images at 30 frames per second.

3.2 Surface material

The surface material used in these trials was quartz sand (98.7 per cent SiO$_2$) with a size range of 1–2.5 mm and a median grain diameter (the grain diameter for which half the sample by weight is smaller and half is larger) of 1.83 mm. The detailed granulometric information is provided in Table 2. With this size range of particles, we do not expect to be sensitive to interstitial air effects.
these have been shown to be negligible for grains with diameters 
>0.1 mm (Pak, Van Doorn & Behringer 1995; Katsuragi 2016).
This is demonstrated specifically for low-speed impacts into a gran-
ular material by Katsuragi & Durian (2007). The individual grain
density is 2.65 grams cm
−3 and each grain has a measured hardness
of 7 Mohs (Fibre Verte 2013).

In order to measure the angle of repose, sand was allowed to pour
from a bottle on to a flat surface. The surface was covered with
the same sand (glued to the surface). The experiment was filmed
and repeated three times. Using the final image, and the measuring
tool in GNU Image Manipulation Program (GIMP), the angle of
repose of the sand on both sides of the pile was measured for each
trial. The resulting angle of repose was found to be 32.5 ± 2.4.
This is a very typical value for sand in a terrestrial environment.
Lunar soil samples have been found, however, to have angles of
repose ranging from 25° to 50° (Carrier, Olhoeft & Mendell 1991);
the higher values are likely due to the more angular particles that
arise from fragments generated from impact comminution. Lunar
regolith simulants, such as JSC-1, therefore contain more angular
particle shapes and have a higher angle of repose than our quartz
sand (∼45°; McKay et al. 1994). Martian regolith simulants, such as
SSC-1 and SSC-2, have also been developed and these have angles
of repose ranging from 35° to 41° (Scott & Saaj 2009). On aster-
oids, gravitational slopes above angles of ∼35° are rare (Thomas
et al. 2002; Scheeres et al. 2006). This indicates that the angle of
repose may be lower for asteroid regolith, despite the Hayabusa
sample return analyses showing that Itokawa regolith particles are
more angular than lunar regolith (Tsuechiyama et al. 2011).

The surface container was filled with ∼80 kg of sand, reaching
a height of ∼17 cm. This gives an approximate bulk density of
1790 kg m
−3. As noted in Sunday et al. (2016), the deceleration
system naturally regulates the bulk density of the surface material,
and the bulk density does not change between trials. The sand was
brushed, however, to restore a level surface before each trial.

4 EXPERIMENTAL TRIALS

4.1 Typical experiment data

Shown in Fig. 3 is a set of typical experiment data. In this example,
the initial separation distance between the sand surface and the pro-
jectile was 2 cm and there were 4.8 kg of counterweights (including
the mass of the counterweight holders). Sensors 1 and 3 were in
the projectile, and sensor 2 was attached to the container. No fil-
tering has been applied to the data. At the start of the experiment,
before the container release, the accelerometers all measure 1g. At
the moment of release, there are extensive vibrations due to the
mechanical release mechanism (for details, see Sunday et al. 2016).
These vibrations are larger for the projectile as, being attached only
by the electromagnetic, it is free to move. After approximately 0.1 s,
there is a large signal recorded by the sensor attached to the surface
container. This is due to the chain falling on to the surface container
(Fig. 4). Next, close to 0.4 s, the low-velocity collision between the
projectile and the sand in reduced gravity can be seen. Finally, at
0.7 s, the surface container impacts the honeycomb material and the
container and projectile rebound until coming to rest.

A good experiment, such as the one shown in Fig. 3, is one in
which the following criteria are met: (1) the chain falls on to the
surface container a sufficiently long time before the projectile–sand
collision, (2) there are no large vibrations of the surface container
due to friction during the projectile–sand collision, and (3) the pro-
jectile comes to rest on the surface of the sand before the surface
container impacts the honeycomb material. The last point, demon-
strated by the projectile and surface container having the same
Figure 4. Chain falling on to surface container. Before release, the surface container is held by a large chain (left-hand image). Upon release, the surface container begins to fall but is slowed down by the counterweights (middle figure). The chain, accelerating faster than the surface container, falls on to the surface container (right-hand figure) causing the vibrations seen at ∼0.1 s in Fig. 3. The time delay between release and the chain hitting depends on the acceleration of the surface container.

Figure 5. Cross-correlation of the two projectile sensors. The location of the maximum value of the cross-correlation indicates the time lead or time lag. In this example, there is a time difference of six samples (5 ms) before the fine synchronization is applied.

acceleration (see Fig. 3, right), indicates that the collision has entirely finished within the period of time of the drop.

In the experiment data, we typically see fluctuations in the projectile acceleration during impact. Some of these fluctuations can be attributed to the accelerometer noise or the variable acceleration of the sand container. However, others are likely due to the creation and annihilation of elements of the force network in the granular material as reported in Goldman & Umbanhowar (2008).

5 DATA ANALYSIS

The primary data source for these experiments is the accelerometers. However, we also make use of the high-resolution images in order to validate the accelerometer analyses. The different processes involved are described below.

5.1 Synchronization of the accelerometers

First, the drop was identified by hand in the accelerometer data and a ∼2 s time period around the drop was extracted from the data of each sensor. As the sensors were not all started exactly simultaneously, a synchronization is necessary. The initial, rough synchronisation of the accelerometers was performed by hand using the moment of release of the sand container (top figure, Fig. 6). Then, a precise synchronization was performed automatically. This involved computing the normalized cross-correlation of the data between pairs of sensors (Fig. 5). The location of the maximum value of the

Figure 6. Synchronization of the sensors. Above: vertical acceleration recorded by the three sensors following a rough synchronization performed by hand with a zoom on the moment of release showing that the data are not perfectly synchronized. Below: vertical acceleration recorded by the three sensors following the fine synchronization performed via cross-correlation, also with a zoom on the moment of release, showing that the data are now synchronized. In this example, sensors 1 (blue) and 3 (orange) were in the projectile and sensor 2 (red) was attached to the container.
Calculation of the collision velocity and penetration depth. Left: the relative acceleration of the projectile and the sand container for the period around the projectile–sand collision. Middle: the relative velocity of the projectile and the sand container for the period around the projectile–sand collision. The maximum values of the relative velocity – the collision velocity – are indicated by the two crosses. Right: the relative displacement of the projectile and the sand container during the collision, i.e., the penetration depth of the projectile into the sand. The maximum penetration distances, as measured by the two sensors, are shown by the dotted lines. The two lines in each figure correspond to the relative values between the sand container sensor (#2) and the two projectile sensors (#1 and #3), as shown in Fig. 3.

Cross-correlation indicates the time lead or time lag that is used to align the time vectors of the two sensors. The synchronization is performed first between the two sensors in the projectile (in the cases where there are two), then the synchronization is performed between one of the projectile sensors and the surface container sensor. The resulting synchronization is precise to within two samples, i.e., <2 ms (lower figure, Fig. 6).

### 5.2 Collision investigation

The approximate collision location is identified in the synchronized accelerometer data. The mean effective acceleration of the sand container during the projectile–sand collision ($g_{\text{eff}}$) is then given by the mean of the sand container acceleration over this period. The peak acceleration ($A_{\text{max}}$) of the projectile is the maximum of the projectile sensor acceleration during the collision with the sand. In Fig. 3 (right), the peak acceleration of the two projectile sensors is indicated by the black and grey crosses.

The moving average of the sand container and projectile acceleration are then calculated as a function of time during the identified time period ($\overline{A}_{\text{box}}$ and $\overline{A}_{\text{proj}}$, respectively). The start of the collision is defined when $\overline{A}_{\text{proj}} > 1.5 \overline{A}_{\text{box}}$, where $\overline{A}_{\text{box}}$ is the mean standard deviation of the projectile sensor during free-fall. The end of the collision is defined when $\overline{A}_{\text{proj}} < \overline{A}_{\text{box}} + Y \sigma_{\text{box}}$, where $\sigma_{\text{box}}$ is the standard deviation of the moving average of the sand container acceleration and $Y$ varies between 0.35 and 1.5 depending on the ratio of the peak acceleration to the mean effective acceleration of the sand container. The collision duration ($\tau_c$) is then the difference between the collision start and end times. In Fig. 3 (right), the collision duration calculated from each of the projectile sensors is indicated by the black and grey horizontal dashed lines.

The vibrations measured during the sand container release can be large enough to saturate the projectile accelerometer(s) as can be seen clearly for sensor 3 in Fig. 3 (left). Due to this, and the fact that the falling chain provides additional vibrations on the sand container accelerometer, it is not possible to simply integrate the accelerometer data of each sensor from the start of the experiment in order to find the relative velocity between the projectile and the sand at the time of the collision. Instead, a different approach is used.

The relative acceleration of the projectile and the sand container is calculated from the moving average accelerations of the projectile and sand container, for the period around the projectile–sand collision ($A_{\text{rel}} = \overline{A}_{\text{proj}} - \overline{A}_{\text{box}}$; Fig. 7, left). The relative acceleration is integrated to give the relative velocity of the projectile and the sand container ($V_{\text{rel}}$). As the projectile remains in contact with the sand at the end of the collision, the relative velocity at the end of the collision should be zero. This information allows the initial relative velocity at the beginning of the time period to be established and thus the relative velocity throughout the collision (Fig. 7, middle). As the projectile immediately starts to slow down upon impact, the collision velocity ($V_{\text{c}}$) is the maximum value of the relative velocity (indicated by crosses in Fig. 7, middle). The relative velocity is then integrated, starting from the instant when the collision starts (Fig. 7, right). This gives the relative displacement of the projectile and the sand container during the collision and is analogous to the penetration depth of the projectile into the sand ($Z_{\text{rel}}$). The maximum relative displacement is therefore the maximum penetration depth of the projectile ($Z_{\text{max}}$, indicated by the dotted lines in Fig. 7, right). The final penetration depth is generally marginally smaller than the maximum penetration depth, due to a slight relaxation of the impact crater following the impact (this can be seen in Fig. 7, right).

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**Figure 7.** Calculation of the collision velocity and penetration depth. Left: the relative acceleration of the projectile and the sand container for the period around the projectile–sand collision. Middle: the relative velocity of the projectile and the sand container for the period around the projectile–sand collision. The maximum values of the relative velocity – the collision velocity – are indicated by the two crosses. Right: the relative displacement of the projectile and the sand container during the collision, i.e., the penetration depth of the projectile into the sand. The maximum penetration distances, as measured by the two sensors, are shown by the dotted lines. The two lines in each figure correspond to the relative values between the sand container sensor (#2) and the two projectile sensors (#1 and #3), as shown in Fig. 3.
Figure 8. Sand container model matrix. The model matrix representing the sand and container visible through the Makrolon front panel. The model matrix has values of 255 (representing the white colour) for the part filled with sand, and 0 representing the black background.

Figure 9. Reference marker identification. Left: the search area to find the multiple reference markers of the sand container is shown in yellow. Middle: for each reference marker, several candidates are found (shown by the different coloured lines). The option with the closest match to the reference model matrix is selected (indicated by the white dashed line). Right: the reference markers identified in the image.

In the trials where there are two sensors in the projectile, such as Fig. 7, the reported values of peak acceleration, collision duration, collision velocity and maximum penetration depth are the mean values of the two measurements and the reported uncertainty is the standard deviation of the two measurements.

5.3 Validation with image analysis

We make use of the images acquired by the high-speed, high-resolution camera to validate the absolute accelerometer measurement, taking the sand container motion as a test case. The image processing flow is based on matrix detection (feature-based tracking). Rather than tracking only one object in the images, several reference markers are tracked, meaning that the results are less sensitive to small inaccuracies in the matrix identification and to pixellization effects.

5.3.1 Marker identification and tracking

As a first step, a model matrix representing the sand and container visible through the Makrolon front panel is defined. The model matrix has values of 255 (representing the white colour) for the part filled with sand, and 0 representing the black background, as seen in Fig. 8. The central column of each image is then divided into sub-matrices with the same dimensions as the model matrix and the Minimum Least Square Error (MLSE) is calculated between the model matrix and each sub-matrix. The sand container can then be identified in the image as the sub-matrix with the minimum MLSE.

The sand container is automatically identified using this method in every 50th image (the full frame rate is not necessary for this first step). The position data of the sand container are then used to generate a dynamical model for the sand container’s motion. As the sand container acceleration is not constant, the acceleration has been modelled as a second-order equation (as the friction varies with the square of the speed) and the speed and the displacement are third- and fourth-order equations.

Once the coordinates of the sand container have been automatically obtained from the previous step, a search area to find the multiple reference markers of the sand container can be defined as shown in Fig. 9 (left). The model reference marker is a rectangular white matrix. As for the sand container search algorithm, the search area is divided into sub-matrices with the same dimensions as the model matrix and the MLSE is calculated between the model matrix and each sub-matrix. From this search, several candidate reference markers appear as each reference marker is identified several times (see Fig. 9, middle). The best fit for each reference marker amongst the candidates is selected by grouping the candidates according to their coordinates and selecting the option with the minimum error (represented by the white dashed line in Fig. 9, middle). Using this method, and the dynamical model to reduce the search area as described above, the reference markers are identified in each image (see Fig. 9, right).
5.3.2 Motion estimation

Once the markers have been identified in every image, the coordinates of the top left pixel of each reference marker are recorded allowing the displacement in pixels to be calculated. The displacement of the sand container is then the mean displacement of all of the reference makers and the velocity is the time derivative of the mean displacement. By measuring the sand container width in the images, the pixel scale was determined to be 5 pixels per cm. Fig. 10 compares the displacement and velocity of the sand container as a function of time, calculated from the image and accelerometer analysis. The two independent methods show a good agreement for both the velocity and the displacement. However, as the process of numerical differentiation introduces more errors than integration, the displacement determined from the accelerometer data is more accurate than the acceleration determined from the image-based displacement data. In fact, the acceleration data is not shown here because small fluctuations in the image-based displacement and velocity result in large fluctuations after differentiation. The accelerometer data, therefore, will be used for the remaining analysis.

6 RESULTS

Fig. 11 gives the range of experiments performed. The range of experiments performed is limited due to the experimental set-up; at low effective accelerations and high collision velocities, the experiment drop height is the limiting factor. At low collision velocities and higher effective accelerations, the initial separation between the projectile and the sand surface is the limiting factor. This is discussed in detail in Sunday et al. (2016). The range of the performed trials, compared to the ranges of other Atwood machine collision experiments and the theoretical calculations of the ISAE-SUPAERO drop tower (presented in Sunday et al. 2016), is given in Fig. 11, right. The main reason for the differences between the theoretical experiment range and the actual experiment range is the friction in the drop tower guide rails; as the sand container accelerates slightly slower than in the case where there is no friction, the projectile–sand collision occurs sooner and the relative velocity is smaller. As the in situ effective acceleration is measured directly by the surface container accelerometer, the variation from the theoretical results only has consequences for the experiment planning (choice of counterweight masses, choice of drop height to ensure that the collision is centred in the camera field of view,...) but does not affect the scientific results. The measured range of the trials confirms that we have developed a robust experimental method for performing low-velocity collisions in reduced gravity.

The peak acceleration measured by the projectile sensors during the collision with the sand surface has the strongest dependence on the collision velocity and scales with the square of the collision velocity (Fig. 12). At the lower collision velocities, the peak is not pronounced, but is rather a broad maximum (as also observed by Goldman & Umbanhowar 2008). The trend of increasing peak acceleration with collision velocity is clearly visible in both the unnormalized and normalized peak acceleration data (Fig. 12). The peak acceleration does not tend to zero as the collision velocity approaches 0 cm s\(^{-1}\). This non-zero intercept indicates a force dominated by friction; frictional/hydrostatic forces dominate at very low collision velocities, compared to higher velocities where hydrodynamic forces dominate (see discussion in Section 7).

Fig. 13 shows the peak acceleration measured by the projectile sensors during the collision with the sand surface, as a function of the effective gravity, i.e. the measured acceleration of the
Figure 11. Experiment range. Left: the range of the experimental trials performed. At low effective gravities and high collision velocities, the experiment is limited by the experiment height. At high effective gravities and low collision velocities, the experiment is limited by the initial separation between the projectile and the sand. See Sunday et al. (2016) for details. The hollow markers show trials where there was only one functioning accelerometer in the projectile. The solid markers show trials where there were two functioning accelerometers in the projectile, and the error bars indicate the standard deviation of the two measurements. Error bars are not shown for the effective acceleration as there was only one accelerometer attached to the surface container for these trials. Right: relative regimes accessible from known Atwood machines (for details, see Sunday et al. 2016). Also shown (red crosses) are the trials that have been performed here.

Figure 12. Peak acceleration and collision velocity. Left: peak acceleration of the projectile as a function of the collision velocity. Right: peak acceleration of the projectile normalized by the effective gravity as a function of the collision velocity. The markers are colour-coded to indicate the effective gravity, as shown in the colour bar. The solid and hollow markers have the same significance as in Fig. 11. The dashed grey lines in the figures show the following fits to the data: $A_{\text{max}} = 57.9 V_c^2 + 1.3$ and $A_{\text{max}}/g_{\text{eff}} = 66.9 V_c^2 + 2.8$, respectively.

The collision duration ranges from $\sim 70$ to $\sim 210$ ms but is independent of both the effective gravity and the collision velocity (Fig. 14). Our data indicate that the maximum penetration depth is also independent of the effective gravity but scales linearly with the collision velocity. The acceleration profile of the projectile always reaches a maximum (for lower velocities, the maximum can be very broad) before reducing to the level of the surface container (see Fig. 3 for an example). As the projectile and the surface container have the same acceleration at the end of the experiment, this indicates that the collision has entirely finished within the period of time of the drop.

1 To verify the linear dependence, a generic model $Z_{\text{max}} = a V_c^n + \beta$ has been tested with 200 values between 0 and 2. The minimum least squares error corresponds exactly to $n = 1$. 
Figure 13. Peak acceleration and effective gravity. Left: peak acceleration of the projectile as a function of the effective gravity (the measured acceleration of the surface container). Right: peak acceleration of the projectile normalized by the effective gravity as a function of the effective gravity. The markers are colour-coded to indicate the collision velocity, as shown in the colour bar. The solid and hollow markers have the same significance as in Fig. 11.

Figure 14. Collision duration. Left: collision duration as a function of the effective gravity. The markers are colour-coded to indicate the collision velocity, as shown in the colour bar. Right: collision duration as a function of the collision velocity. The markers are colour-coded to indicate the effective gravity, as shown in the colour bar. The solid and hollow markers have the same significance as in Fig. 11.

Figure 15. Penetration depth. Left: maximum penetration depth as a function of the effective gravity. The markers are colour-coded to indicate the collision velocity, as shown in the colour bar. Right: maximum penetration depth as a function of the collision velocity. The markers are colour-coded to indicate the effective gravity, as shown in the colour bar. The dashed grey line shows the best linear fit to the data: $Z_{\text{max}} = 0.07V_c + 0.03$. The solid and hollow markers have the same significance as in Fig. 11.
Also, as the projectile acceleration does not return to 0 m s$^{-2}$, the projectile does not return to free-fall and, therefore, left contact with the sand surface. In all of the experimental trials performed here, no rebound was observed and the coefficient of restitution is thus zero.

7 DISCUSSION

The drag force during penetration into a granular can be separated into two terms: the hydrodynamic drag force and the static resistance force (e.g., Allen, Mayfield & Morrison 1957). If the drag force scales with the square of the collision velocity, this indicates that the impact is occurring in the inertial (or hydrodynamic) regime. In other words, the grains have become sufficiently fluidized during the impact for the system to display inertial, fluid-like drag. On the other hand, a small or zero dependence of the drag force on the collision velocity would indicate a quasi-static (or hydrostatic) regime.

In our experiments, the peak accelerations (and thus the drag force) scale as $A_{\text{max}} = 57.9V_c^2 + 1.3$, where the units of $A_{\text{max}}$ and $V_c$ are m s$^{-2}$ and m s$^{-1}$, respectively (see Fig. 12). Therefore, for collision velocities of $\geq 15$ cm s$^{-1}$, the hydrodynamic drag dominates and the collisions occur in the inertial regime, and for collision velocities of $\leq 15$ cm s$^{-1}$, the static resistance force dominates and the collisions occur in the quasi-static regime. For the regime transition to occur at such low velocities is a surprising result. Goldman & Umbanhowar (2008), for example, found that under terrestrial gravity, the quasi-static to inertial regime change occurs at collision velocities an order of magnitude larger: the peak acceleration of two steel spheres ($\sim$2 kg and $\sim$80 g) impacting glass beads scales with the square of the collision velocity for velocities $\geq 1.5$ m s$^{-1}$, but not for the lower collision velocities. In the same experiments, this regime change was also evident in the collision durations: the collision time is independent of the collision velocity at the higher collision velocities (in the inertial regime), but for lower collision velocities ($\leq 1.5$ m s$^{-1}$), the collision duration increases with decreasing collision velocity indicating the quasi-static regime. Here we find that the collision duration is independent of the collision velocity (such as in the higher energy collisions of Goldman & Umbanhowar 2008), further indicating the importance of the inertial regime in our experiments.

One explanation for the regime change occurring at collision velocities an order of magnitude smaller in our experiments (and impact energies two orders of magnitude smaller) is the different surface materials used. In our experiments, the quartz sand is more irregular and frictional than the glass beads used by Goldman & Umbanhowar (2008) (yet still much less angular than the samples returned from asteroid; Itokawa; Tsuchiyama et al. 2011). The hydrodynamic drag will therefore be of greater importance here than in their experiments. The same applies if we compare our results to those of Altshuler et al. (2014) who studied a sphere impacting polystyrene beads. Given the impact velocities of $\sim$1 m s$^{-1}$ and the small hydrodynamic drag coefficient of polystyrene beads, they estimate the hydrodynamic drag in their experiments and simulations to be negligible. The different surface materials, therefore, also explain why we find the collision duration to be independent of the effective gravity, whereas both Altshuler et al. (2014) and Goldman & Umbanhowar (2008) found that the collision duration scales with $g_{\text{eff}}^{1/2}$.

An alternative, or perhaps additional, explanation can be found by recalling that the quasi-static resistance force is proportional to the object’s cross-section times the local pressure (Albert et al. 1999). As the local pressure is directly related to the gravitational acceleration, the quasi-static resistance force should tend to zero as gravity is reduced. Katsuragi & Durian (2007) also suggest that the quasi-static force is linearly proportional to gravity in granular impact cratering experiments. Therefore, in the absence of gravity or a confining pressure, the quasi-static regime does not exist and the drag force should scale with the square of the velocity for any velocity range, not just for the high-energy impacts. This was also observed by Seguin et al. (2016) who performed numerical simulations of a sphere moving through a cloud of grains. They explain that, no gravity acts and no external pressure is imposed from any external boundary, no stress scale exists except the kinetic pressure ($\rho V^2$) arising from the collision processes. The quasi-static regime, therefore, is expected to reduce as the effective gravity becomes lower. We indeed observe that the quasi-static to inertial regime transition occurs for much lower impact energies in our low-gravity experiments compared to similar experiments performed under terrestrial gravity.

Our data indicate that the maximum penetration depth is independent of the effective gravity (as also found by Altshuler et al. 2014) but scales linearly with the collision velocity. The linear scaling of penetration depth with impact velocity was also found by Goldman & Umbanhowar (2008) and de Bruyn & Walsh (2004) for higher velocity ($>$1 m s$^{-1}$) impact experiments in which the penetration depth is generally greater than one projectile radii. We show here that at low effective gravities, the linear scaling is also valid for shallow impacts of an aluminium sphere into sand. The projectile has a diameter of 10 cm and the maximum penetration depth observed in the experiments is $\sim$1/4 of the projectile diameter.

8 CONCLUSIONS

Making use of our novel drop tower facility (Sunday et al. 2016), we have performed low-velocity (2–40 cm s$^{-1}$), shallow impact experiments of a 10 cm diameter aluminum sphere into quartz sand in low effective gravities ($\sim$0.2–1 m s$^{-1}$). A total of 46 trials were performed, of which 41 were classified as acceptable trials and subsequently analysed. No rebounds are observed in the experimental trials and the coefficient of restitution is thus zero. We find that the penetration depth scales linearly with the collision velocity but is independent of the effective gravity for the experimental range tested, and that the collision duration is independent of both the collision velocity and the effective gravity.

During similar impact experiments under terrestrial gravity, the transition from the quasi-static regime (where the static resistance force dominates) to the inertial regime (where hydrodynamic effects dominate) occurs at collision velocities of $\sim$1.5 m s$^{-1}$ (Goldman & Umbanhowar 2008). Our low-gravity experimental results indicate that the collisions occur in the inertial regime down to collision velocities of $\sim$15 cm s$^{-1}$; equivalent to an impact energy two orders of magnitude smaller than the terrestrial gravity experiments. The lower energy regime change may be due to the increased hydrodynamic drag in our experiments, but may also support the notion that the quasi-static regime is expected to reduce as the effective gravity becomes lower. The latter indicates that in the absence of gravity or a confining pressure, the quasi-static regime does not exist and the drag force scales with the square of the velocity for any velocity range, not just for high-energy impacts.

To investigate the reason(s) for the lower energy regime change found here, further low-gravity experiments should be performed with different surface materials. It would also be useful to perform
experiments at similar collision velocities over a large range of effective gravities; a challenging task given the range of experimental conditions accessible in our drop tower (Fig. 11). Numerical simulations (e.g. Holsapple 1993; Sánchez & Scheeres 2011; Schwartz, Richardson & Michel 2012), validated using the experimental data obtained in these trials, may be a complementary approach for such studies. The numerical simulations could also be used to extrapolate our results to even lower gravity regimes, inaccessible with our drop tower. For comparison, the smallest effective gravity obtained in these experiments is just less than that of asteroids (1) Ceres and (4) Vesta, with surface gravities of \( \sim 0.29 \) and \( \sim 0.25 \text{ m s}^{-2} \), respectively. The \( \sim 17 \text{ km asteroid (433) Eros} \) has a surface gravity one hundred times smaller than the smallest effective gravity tested here, and the surface gravity of (25143) Itokawa (\( \sim 300 \text{ m} \)) is yet another hundred times smaller. On the other end of the scale, the largest effective acceleration that has been tested in these experiments (\( \sim 1 \text{ m s}^{-2} \)) is comparable to the surface gravity of Saturn’s moon Enceladus.

Finally, in order to improve the data analysis, it may be possible to combine both the images and the accelerometer data. By using information theory (e.g. Khaleghi et al. 2013), the combination of relevant information from these two data sources may provide an even more reliable measure of the motion of both the surface container and the projectile.

9 IMPLICATIONS FOR SMALL BODY SPACE MISSIONS AND FOR ASTEROID EVOLUTION

Current and future asteroid landers (MASCOT, MASCOT-2, MINERVA, AGEX; Tsuda et al. 2013; Ho et al. 2016; Karatekin et al. 2016) will be deployed on ballistic trajectories to the surface of asteroids, with no attitude control. If, during their low-velocity landing, there is no rebound (as was the case in these experiments), the lander would remain at the location of the initial touchdown. This places even more importance on the precision of the deployment strategy from the main spacecraft for the landers without mobility mechanisms. However, this would also reduce the risk of the lander rebounding and being lost to space, and would simplify the lander design as specific areas of the asteroid surface could be targeted (e.g. choosing a region with the best thermal conditions for the payload operations in order to minimize, as far as possible, complex thermal regulation; Cadu et al. 2016).

Our experiments suggest that the landing velocity is the critical parameter that will influence both the penetration depth and the acceleration profile during landing. The peak accelerations observed varied from \( \sim 1 \) to \( 12 \text{ m s}^{-2} \) and the maximum penetration depth observed in the experiments was \( \sim 1/4 \) of the projectile diameter. However, a harder, or denser, surface material is likely to lead to larger peak accelerations and a smaller penetration depth, whereas a more fluffy regolith may reduce the peak accelerations while increasing the penetration depth. The variation of peak accelerations and penetration depth with surface properties (for example, particle size, density, cohesion, angularity and frictional properties) in low gravity should be studied in future experiments in order to cover as many asteroid surface materials as possible. Similarly, for shallow penetrations, the projectile shape is known to play crucial role, with sharper objects penetrating deeper (Newhall & Durian 2003). Further experiments are therefore needed to understand the influence of the projectile shape in low-velocity and low-gravity collisions. This is also particularly important since asteroid landers are often rectangular rather than spherical in shape (e.g. Ho et al. 2016; Karatekin et al. 2016).

The observed penetration rather than rebounding also has implications for asteroid surfaces. As discussed in Nakamura et al. (2008), two types of low-velocity impact can occur naturally on asteroids: the impact of remnant small ejecta from a catastrophic disruption event and the secondary impact of ejecta blocks from a primary impact on the surface. The collision dynamics between the impacting ejecta and the regolith on an asteroid surface determines whether the debris will bounce, penetrate fully or partially into the surface or remain on the surface. Our results support the findings of Nakamura et al. (2013) showing that the isolated large blocks on the smooth terrains of Itokawa (e.g. Nakamura et al. 2008) could be ejecta blocks that collided with the surface during re-accumulation, but did not deeply penetrate. If the inertial regime dominates on asteroid surfaces, the penetration depth of ejecta from cratering events will also be shallow and will be directly linked to the re-impacting velocity of the ejecta.

More extensive fluidisation has been observed in micro-gravity following changes in the granular force contact network, compared with identical experiments under terrestrial gravity (Murdock et al. 2013), and avalanches have been found to be longer range at lower gravity (Kleinhans et al. 2011). The notion of a reduced quasi-static regime in very low gravity would support the enhanced fluidisation observed in these experiments. This may imply that regolith material becomes more easily fluidized for lower energy events such as small micro-meteoroid impacts (e.g. Richardson et al. 2005; Garcia, Murdock & Mimoun 2015). We emphasize, however, that the results presented here are for one experimental configuration only and should be developed further (as mentioned above) to determine more precisely the role of the surface material properties, the impactor properties and gravity.

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