Magnetisation reversal in Ising ferromagnet by thermal and field gradients

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Abstract

We report the results of the magnetisation reversal in Ising ferromagnet having thermal and field gradients by Monte Carlo simulation. We have studied the distribution of reversal times for different values of thermal and field gradients and compared the results with those obtained for uniform temperature. The movement of the domain wall of distinct domains and the growth of roughness of domain wall have also been studied statistically. The role of competing thermal and field gradients, in the reversal mechanism, was also studied and a line of marginal competition was obtained.

Keywords: Statistical physics

1. Introduction

The Ising model is a prototype to study the thermally activated process like nucleation [1, 2]. In the paramagnetic region, each spin has almost equal probability of finding itself in the up or down state. As a result, almost equal number of up and down spins are available in the system. However, in the ferromagnetic region (below the critical temperature), the system prefers to remain in either of two states: one state having positive magnetisation where most of the spins are up, and the other state having negative magnetisation. For a system with finite size, the spontaneous
reversal of magnetisation (where the magnetisation changes sign) occurs due to thermal noise. This phenomenon could be observed if the system is studied over a prolonged period of time.

This magnetisation reversal has a technological application in designing the magnetic recording devices. In this recording device, for high recording speed, external field driven rapid reversal of magnetisation is required. Let us briefly mention a few studies, related to the field driven reversal of magnetisation, in Ising ferromagnets. The large scale computer simulation in Ising ferromagnet was studied [3] to identify the distinct regimes of single droplets and multi-droplets as a precursor of magnetisation reversal. The problem of classical nucleation is still challenging. A significant amount of work has already been done [4, 5, 6, 7] in this field. However, all the studied mentioned, so far, have been done for steady (in time) and uniform (over the space) magnetic field.

The direction of research in the field of nucleation has recently been steered towards the time dependent magnetic field. The magnetisation reversal transition was studied [8] in Ising model driven by an impulsive magnetic field and a phase boundary has been drawn. Recently, the nucleation and magnetisation reversal have been studied [9] in Ising ferromagnet driven by a field spreading in time. Here the competing effects of reversal time and the rate of spreading have been discussed. The effects of the rate of changing the temperature on the reversal time was investigated [10], recently. The magnetisation switching in classical Heisenberg model for small ferromagnetic particles was studied extensively [11]. The experimental evidences of magnetisation switching has also been reported [12]. In these cases, the magnetic field was uniform over the space.

What happens when the applied field has a spatial variation, can be a triggering question. Very recently, the magnetisation reversal in Ising ferromagnet by a field having a spatial gradient, was studied [13] by extensive Monte Carlo simulation. In that case, the temperature of the system was uniform. In this paper, we have studied the magnetisation reversal, in Ising ferromagnet, where the system has a nonuniform spatial distribution of temperature.

In this article, we report the results of our studies on systems having non-uniform spatial distribution of temperature along with the simultaneous presence of spatially distributed non-uniform external magnetic field. The paper is organised as follows: In the next section, section 2, we have described the model, the results of the simulation are reported in section 3, the paper ends with a discussion in section 4.
2. Model

The Hamiltonian of a two dimensional Ising ferromagnet with nearest neighbour interaction and in presence of magnetic field (which can vary spatially) can be represented as,

\[ H = -J \sum_{<i,j>} S_iS_j - \sum_i h(i)S_i \]  

(1)

Here \( S_i (= \pm 1) \) represents the Ising spin at i-th lattice site. \( J (> 0) \) is the ferromagnetic interaction strength and \( h(i) \) is the external magnetic field at the i-th lattice site.

In the first part of our work, we have considered the uniformly applied magnetic field and the temperature has a spatial variation along the x direction only), instead of the considering the spatially uniform (temperature) cases in the previous studies [3, 9, 13]. As a result there is a gradient in temperature between the temperature of the left edge and the right edge of the lattice. We have considered the linear variation of the temperature as:

\[ T(x) = g \ast x + c, \]  

(2)

where, \( T(x) \) is the temperature of the x-th column of the square lattice. The thermal gradient is defined as, \( g = \frac{dT(x)}{dx} \).

If initially, \( T_l \) and \( T_r \) are the assigned temperatures on the left boundary and the right boundary of the lattice respectively, the thermal gradient, \( g \) can be calculated as \( g = (T_r - T_l)/L \). The constant \( c \) (in equation (2)) will be equal to \( T_l \). Here all the magnetic fields are measured in the units of \( J \).

In this study, we have fixed \( T_l = 1.4 \ J/k_B \) and have varied \( T_r \) at values less than \( 1.4 \ J/k_B \) to set the desired thermal gradient, in the system.

In the second part of our study, we have the temperature gradient as described. In addition to that, we have introduced a field gradient in the system. Let \( h_l \) and \( h_r \) be the applied magnetic fields on the left and the right boundaries of the lattice respectively. The magnetic field varies linearly between the two boundaries. So the field takes the form:

\[ h(x) = f \ast x + d \]  

(3)

where, \( f = \frac{dh(x)}{dx} \) is the field gradient. We have thus introduced both gradients of the field and temperature in this part of our study. Needless to say that \( d = h_l \) (in equation (3)).

We have kept \( h_r \) fixed at \(-0.5\) and varied \( h_l \) to get the required field gradients.
3. Calculation

In this simulation, we start with a two dimensional lattice of size $L \times L$. We use open boundary conditions in all directions. Initially, we have considered, $S_i = +1 \forall i$ (perfectly ordered state). Next, at each time step, we follow random updating method. We select any site randomly. Calculate the change in energy $H$ (equation (1)) for that spin to flip ($S_i \rightarrow -S_i$). Let that energy be $\Delta H$. The probability that the randomly selected spin will flip, is given by the Metropolis formula [14]:

$$P = \text{Min}(1, \exp(-\Delta H / k_B T(i, j)))$$

The temperature $T(i, j)$ (at any site $(i, j)$) is measured in the unit $J / k_B$, where $k_B$ is the Boltzmann constant.

The scheme of the simulation can be described briefly as follows: A random number (uniformly distributed between 0 and 1), $r$, is called. If this random number $r$ is less than or equal to Metropolis flipping probability $P$ then flipped the selected spin. In this way, $L^2$ such spin were flipped in random updating scheme. This $L^2$ number of spin flips is taken to be a single time step and defined as one time unit (Monte Carlo Step per Spin or MCSS).

For our work, we have chosen $L = 300$. The reason behind this choice is a compromise between the affordable computational time and to have the clear observation of distribution of metastable lifetimes.

4. Results

4.1. Presence of thermal gradient only

Initially, the system is kept in a fully magnetised state ($S_i = +1 \forall i$). There is an external magnetic field applied in the opposite (to the direction of initial magnetisation) direction. Then the minimum time taken by the system to reach a negative magnetisation state from the completely ordered initial state of positive magnetisation, in the presence of the applied external magnetic field is called the reversal time or the metastable lifetime of the ferromagnetic system. Figure 1a shows the variation, of the magnetisation of such a system, with time.

We have studied the reversal of magnetisation of the system having the thermal gradient (but in the presence of uniform magnetic field). For different values of the thermal gradient, such variations of magnetisation with time, are shown in Figure 1a, b, c and d.

It is observed that as the thermal gradient of the system increases, the reversal time of the system also increases. The distributions of reversal times, obtained over 50,000 such different samples, are shown in Figure 2 for different values of thermal gradient (where the external magnetic field remaining the same $h = -0.5$). The distribution
Figure 1. Variations of magnetisation with time. Starting from top (a) The system at uniform temperature \(T(i,j) = 1.4\). (b) The system with \(T_l = 1.4\) and \(T_r = 1.2\). (c) The system with \(T_l = 1.4\) and \(T_r = 1.0\). (d) The system with \(T_l = 1.4\) and \(T_r = 0.8\), where \(T_l\) and \(T_r\) are the temperatures on left boundary and right edge of the lattice respectively. Temperatures are measured in the units of \(J/k_B\).

Figure 2. Distributions of reversal time of 50,000 ferromagnetic samples for different thermal gradients. Top left (a) The system at uniform temperature \(T = 1.4\). Top right (b) The system with \(T_l = 1.4\) and \(T_r = 1.2\). Bottom left (c) The system with \(T_l = 1.4\) and \(T_r = 0.0\). Bottom right (d) The system with \(T_l = 1.4\) and \(T_r = 0.8\), where \(T_l\) and \(T_r\) are the temperatures on left and right edges of the lattice respectively. Temperatures are measured in the units of \(J/k_B\).
Figure 3. Variations of average reversal time and standard deviation of reversal time with thermal gradient. **Starting from top** (a) Average reversal time varies with gradient as $y \sim \exp(c \cdot x)$. (b) Standard deviation of reversal time varies with gradient as $y \sim \exp(c' \cdot x)$. Thermal gradients are measured in the units of $J/k_B$.

is unimodal and the most probable reversal time increases as the thermal gradient increases. Moreover, the distributions get wider for higher values of the thermal gradient. We have found that the average reversal time (Figure 3a) and its standard deviation (Figure 3b) increases exponentially as the thermal gradient increases when the magnetic field is uniform.

The morphology (i.e., the snapshot of the spin configurations of the lattice at a particular instant of time) of the samples are studied by observing the microstates (at the time of reversal) for different values of the temperature gradient. As Figure 4a shows, in the presence of uniform temperature and field, the lattice morphology at the time of reversal, shows the formation of multiple droplets (small clusters of down spins marked by black dots), distributed almost homogeneously throughout the lattice. However, in the presence of a thermal gradient, keeping the field constant, instead of the homogeneous distribution of the clusters, droplets of down spins tend to assemble near the boundary having higher temperature. And upon increasing the gradient, we observed that, at the time of magnetisation reversal, a rough interface (domain wall) forms, which separates the regions or domains of positive and negative
Figure 4. Snapshots of the spin configurations at reversal time for different sets of temperature gradients. **Top left** a) The system at uniform temperature $T = 1.4$. **Top right** b) The system with $T_l = 1.4$ and $T_r = 1.0$. **Bottom left** c) The system with $T_l = 1.4$ and $T_r = 0.7$. **Bottom right** d) The system with $T_l = 1.4$ and $T_r = 0.2$, where $T_l$ and $T_r$ are the temperatures on left and right edges of the lattice respectively. Temperatures are measured in the units of $J/k_B$. Here, the black dots represent down spins.

The roughness of the interface was observed to decrease (or the interface gets smoother) as the thermal gradient increases. As Figure 4d shows, for a high value of the thermal gradient, the lattice morphology shows two prominent domains of up and down spins, with a smooth interface.

To sketch the shape of the interface (a curved line in two dimensions), we employed the following method: On a particular row, for each spin on that row, we checked the values of its 10 nearest neighbours on both sides. From Figure 4d, we can say that, at any position on interface, almost all the spins to its left will be down spins (as the temperature of the left edge of the lattice is higher) and almost all the spins to its right are up spins. When for a particular spin (in a particular row), both the number of up spins among its 10 neighbours (to its left) and down spins among its 10 neighbours (to its right) are greater than or equal to 8, we fix that spin position as the x-coordinate of interface on that row. In this way the positions (the x-coordinate only) of all the 300 rows of the lattice are noted. In this way we have sketched the shape of the interface.
Figure 5. Distributions of average location of interface (done over 500 samples) for different thermal gradients. **Top left** (a) The system with $T_l = 1.4$ and $T_r = 0.8$. **Top right** (b) The system with $T_l = 1.4$ and $T_r = 0.6$. **Bottom left** (c) The system with $T_l = 1.4$ and $T_r = 0.4$. **Bottom right** (d) The system with $T_l = 1.4$ and $T_r = 0.2$, where $T_l$ and $T_r$ are the temperatures on left and right edges of the lattice respectively. Temperatures are measured in the units of $J/k_B$.

The average of all the x-coordinates (or positions) is the measure of average position of the interface (or domain wall). And the variance of all these x-coordinates may act as a measure of roughness of the domain wall.

The unnormalised distribution of interface positions for different gradients (in the form of histogram) is also consistent with the obtained results. If the gradient is increased the width of the distribution decreases (Figure 5). This observation also provides the testimony to the phenomenon of increasing smoothness of the interface with increasing gradient. One can compare Figures 4 and 5.

From the plot of the average position of the interface (averaged over 500 different samples) versus thermal gradient, it is seen that the average interface position increases up to a certain value and then remains almost fixed to a value near the vertical central line of the lattice (Figure 6a). This displacement of the mean position of domain wall turns out to be a hyperbolic tangent function of the thermal gradient (Figure 6a).
Figure 6. Variations of average position of the interface and the variance of interface position with thermal gradient. Starting from top (a) Average interface position varies with gradient as $y = A \tanh(bx)$. (b) Standard deviation of reversal time varies with thermal gradient as $y = C \exp(-dx)$. Thermal gradients are measured in the units of $J/k_B$.

The plot of the variance in the position of the interface versus the thermal gradient is shown in Figure 6b. It is observed that the variance decreases exponentially (Figure 6b) with field gradient. The variance in boundary position is a good measure of the boundary (of the domain wall) roughness. The observation that the variance decreases with increasing gradient supports the fact that the boundary roughness decreases drastically with increasing gradient. This inference is consistent with our observations of the lattice morphologies of Figure 4 which also showed the decrease in boundary roughness with increasing gradient.

4.2. Simultaneous presence of thermal and field gradients

Here, we maintain the thermal gradient having the form of equation (2). In addition to that we have introduced a field gradient having the form of equation (3).

In our study, $T_l$ is kept fixed at $1.4 \ J/k_B$, while $T_r$ is varied at values less than $1.4 \ J/k_B$. Also, $h_r$ is kept fixed at $-0.5$ and $h_l$ is varied at values higher than
Figure 7. The evolution of the lattice morphology with time for a system where $T_l = 1.4$, $T_r = 0.9$, $h_r = -0.5$, $h_l = -0.4$. **Top left** (a) The system at $t = 100$. **Top right** (b) The system at $t = 200$. **Bottom left** (c) The system at $t = 284$ (Reversal Time). **Bottom right** (d) The system at $t = 750$. Temperatures are measured in the units of $J/k_B$ and fields are measured in units of $J$.

Now, at regions having higher temperature, spins have a higher probability of flipping. Also at regions having higher magnitude of negative field, positive spins have higher probability of flipping. So in assigning a higher magnitude of negative field to the edge having lower temperature and a lower magnitude of negative field to the edge having higher temperature, we have tried to create a situation where the thermal gradient and the field gradient compete with each other in their spin flipping ability.

How does the lattice morphology evolve with time under simultaneous application of thermal and field gradient? We have studied this and our results are shown in Figures 7, 8 and 9.

It is seen that in Figure 7, where the magnitude of the field at $h_l$ is not quite low compared to that of $h_r$, multiple clusters (of down spins) are formed and the size of each cluster grows as the time progresses. But if we decrease the magnitude of $h_l$ compared to that of $h_r$, the number of clusters decreases, (as is evident from
Figure 8. The evolution of the lattice morphology with time for a system where $T_l = 1.4$, $T_r = 0.9$, $h_r = -0.5$, $h_l = -0.2$. **Top left** (a) The system at $t = 501$. **Top right** (b) The system at $t = 701$. **Bottom left** (c) The system at $t = 1025$ (Reversal Time). **Bottom right** (d) The system at $t = 1701$. Temperatures are measured in the units of $J/k_B$ and fields are measured in units of $J$.

Figures 8 and 9). And in Figure 9 where $h_l = 0.0$, only one cluster of negative spin grows. Another way of saying this is as the average magnitude of the negative field decreases, the number of clusters also decreases.

The lattice morphologies at reversal time for these three set of values of temperature and field gradients are compared and shown in Figure 10. It is observed that in Figure 10a, where the field gradient is small and temperature gradient is comparatively large, at reversal time, all the down spins have clustered near the left edge, signifying that the temperature gradient has dominated over the field gradient. But in Figure 10c where the field gradient is high compared to the temperature gradient, at reversal time, all the down spins have clustered near the right edge, signifying the domination of the field gradient over the thermal gradient. However in Figure 10b, an intermediate phenomenon happens where at reversal time, the clustering of down spins does not show notable affinity towards either the right or the left edge. Here both the gradients are competing equally. We may call it marginal competition between field gradient and the thermal gradient. Thus the morphology
Figure 9. The evolution of the lattice morphology with time for a system where $T_i = 1.4, T_r = 0.9, h_r = -0.5, h_l = 0.0$. **Top left** a) The system at $t = 1042$. **Top right** b) The system at $t = 1341$. **Bottom left** c) The system at $t = 2341$ (Reversal Time). **Bottom right** d) The system at $t = 4000$. Temperatures are measured in the units of $J/k_B$ and Fields are measured in units of $J$.

of the lattice at reversal time becomes helpful in indicating which of the gradients dominates over the other. To describe this phenomenon in a quantitative manner, we define a function called the **Competition Factor** ($C_F$).

The morphology in Figure 11a can be taken as a manifestation of complete domination of temperature gradient over field gradient. We take this as our reference lattice. The value of the spin at any site $(i, j)$ on this reference lattice may be denoted by $C(i, j)$. Let $S(i, j)$ represent a spin of any lattice at reversal time. Then the Competition Factor of this lattice is defined as

$$C_F = \left( \sum_{<i,j>} C(i, j) * S(i, j) + (L * L) \right) / (2 * L * L)$$

The morphology shown in Figure 11a will give a $C_F$ (equation (4)) of 1. So it is clear that when Temperature Gradient dominates over field gradient, $C_F$ value will be close to 1. Also the morphology shown in Figure 11b, which shows complete domination of field gradient over the thermal gradient, will give a $C_F$ (equation (4))
Figure 10. The lattice morphologies (at the time of reversal) for different sets of thermal gradient and field gradient. Starting from the top (a) The system with $T_l = 1.4$, $T_r = 0.9$, $h_r = -0.5$, $h_l = -0.4$. (b) The system with $T_l = 1.4$, $T_r = 0.9$, $h_r = -0.5$, $h_l = -0.2$. (c) The system with $T_l = 1.4$, $T_r = 0.9$, $h_r = -0.5$, $h_l = 0.0$. Temperatures are measured in the units of $J/k_B$ and fields are measured in units of $J$.

value of 0. So if a system is dominated by field gradient rather than thermal gradient, the $C_F$ value for the morphology is close to 0. However, if for any system, at reversal time, the lattice morphology gives a $C_F$ close to 0.5, that means for that system, both the gradients are competing almost equally (or marginal competition).
**Figure 11. Starting from the top** (a) The reference lattice morphology used in the calculation of the $C_F$. This lattice morphology is the manifestation of the ideal case where thermal gradient completely dominates over the field gradient (b) This lattice morphology is the manifestation of the ideal case where field gradient completely dominates over the thermal gradient.

**Table 1.** Table showing $C_F$ for different values of thermal and field gradients. The $C_F$ is averaged over 100 samples. Temperatures are measured in the units of $J/k_B$ and fields are measured in units of $J$. The values in the third row are close to the line of marginal competition.

| $T_l$ | $T_r$ | $h_r$ | $h_i$ | Average $C_F$ |
|-------|-------|-------|-------|---------------|
| 1.4   | 0.9   | −0.5  | −0.4  | 0.8313972     |
| 1.4   | 0.9   | −0.5  | −0.3  | 0.7300105     |
| 1.4   | 0.9   | −0.5  | −0.2  | 0.5228405     |
| 1.4   | 0.9   | −0.5  | −0.1  | 0.2742300     |
| 1.4   | 0.9   | −0.5  | 0.0   | 0.2373000     |

This is clearly demonstrated if we keep the thermal gradient constant and change the field gradient gradually from a lower value to higher values. Table 1 shows when the field gradient is small, the thermal gradient dominates and the $C_F$ is close to 1. And when the field gradient rises, the $C_F$ rises, and when the field gradient becomes so high that it dominates over the temperature gradient, the $C_F$ takes values closer to 0.
Figure 12. Line of Marginal Competition: The line which separates the Field gradient Dominated region from the Temperature Gradient dominated region. Here the y axis has an error bar of 0.0003. Temperatures are measured in the units of $J/k_B$ and Fields are measured in units of $J$.

Also in between these two cases, when the influence of both the gradients are almost equal (marginal competition), the $C_F$ is close to 0.5.

So, keeping the temperature gradient constant, if we vary the field gradient, for every value of the temperature gradient, we will find a value of the field gradient (up to an error bar of 0.0003) for which the $C_F$ is 0.5 (up to an error bar of 0.01). Repeating this process several times, we find a set of thermal gradient and field gradient pairs for which the $C_F$ is very close to 0.5, i.e. both the gradients are competing equally (marginal competition). We call the plot of these points the line of marginal Competition (Figure 12). This line separates the region of thermal gradient domination from the region of field gradient domination.

It is worth noting at this point that the Competition Factor is found to be dependent on the lattice morphology at reversal time. It is a worthwhile indicator of which gradient dominates over the other only when the morphology at reversal time is used to calculate the $C_F$. For every system, under any set of conditions, the $C_F$ is 0.5 at the start when all the spins are up, and a long time after reversal when all the spins have flipped, the $C_F$ is again 0.5. Figure 13 shows how the $C_F$ varies with time under 3 different sets of conditions.

5. Discussion

In the first part of this paper, we have investigated the magnetisation reversal (by a uniform negative field) and the evolution of the lattice morphology of a two dimensional Ising ferromagnet under the influence of a thermal gradient. For our work we had fixed the temperature of one edge of the lattice while varying the
Figure 13. Variation of $C_F$ versus time under 3 different sets of Temperature and Field Gradients (Temperature Gradient Dominated, Field Gradient Dominated, and Intermediate). The arrows mark Reversal Times. Temperatures are measured in the units of $J/k_B$ and Fields are measured in units of $J$.

temperature of the other edge at values less than the fixed one. We have observed that the average reversal time increases exponentially with increasing gradient. Also, as the reversal time increases, the variance in the reversal time increases. Then we proceeded to study the lattice morphologies of the system at the time of reversal, for different values of the thermal gradient. It has been found that for the high value of the thermal gradient, the lattice morphology shows two distinct domains of up and down spins, separated by a domain wall. This domain wall becomes smoother as the thermal gradient increases.

In the second part, on top of the thermal gradient, already present, we simultaneously introduce a field gradient in the system. The edge of the lattice having higher temperature is assigned a negative field of lower magnitude. On the other hand, the other edge of the lattice having lower temperature is assigned a negative field of higher magnitude. Thus we created a situation in which both the gradients were made to compete with each other in their spin flipping capability. Looking at the lattice morphologies at reversal time, for different values of the thermal and field gradients, we can identify which of the two gradients dominated over the other. We defined a mathematical function called the Competition Factor, which, taking into account, the lattice morphology at reversal time, gives a dimensionless number lying between 0 and 1, the value of which determines whether the field gradient dominates or the thermal gradient dominates. Using this function, we found out a set of thermal and field gradient duplets for which both the gradients compete with almost equal strength. We made a plot of such points and called it the line of marginal competition. This line separates the region where thermal gradient dominates from the region dominated by the field gradient.
An interesting question may arise regarding the effects of boundary conditions on the roughness of domain wall. In our study, we have used the open boundary conditions in all directions. The directions of both the thermal and field gradients, in our study, are taken along the horizontal axis. As a result, the values of temperature and field are different in the left and right edges of the lattice. In a particular column of the square lattice considered here, the temperature and the fields remain constant. So, it would not be justified to apply periodic boundary conditions horizontally. However, it is possible to apply periodic boundary condition along the vertical direction. Further extensive investigations are required to check whether the application of such type of periodic boundary condition (along the vertical direction only) affects the results or not.

The time of reversal of magnetisation will increase as the size of the lattice ($L$) increases. That has already been reported [3] in the case of uniform field and temperature. We believe, in this case the larger system will increase the time of reversal only. However, this will not remarkably change the qualitative behaviours upon which we have based our inferences.

The magnetisation reversal in ferromagnetic systems has variety of practical uses. This time of magnetisation reversal is an important parameter for the technologies of magnetic recording and storage device [15]. Increase in the reversal time increases their longevity. In the earlier work [13], it was shown that increasing the field gradient can result in the increase in reversal time. But in practice, setting up a field gradient in these devices is difficult. But it would be easier to set up a thermal gradient and tune it to tune the reversal time. Also if we have simultaneous thermal and field gradient, we have an added degree of freedom, a much more versatile tool in our hand to tune the reversal time.

**Declarations**

**Author contribution statement**

Ranajay Datta: Performed the experiments; Wrote the paper.

Muktish Acharyya: Conceived and designed the experiments; Analyzed and interpreted the data; Wrote the paper.

Abyaya Dhar: Contributed reagents, materials, analysis tools or data.

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Additional information

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