Gene and Network Analysis of Common Variants Reveals Novel Associations in Multiple Complex Diseases

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ABSTRACT Genome-wide association (GWA) studies typically lack power to detect genotypes significantly associated with complex diseases, where different causal mutations of small effect may be present across cases. A common, tractable approach for identifying genomic elements associated with complex traits is to evaluate combinations of variants in known pathways or gene sets with shared biological function. Such gene-set analyses require the computation of gene-level P-values or gene scores; these gene scores are also useful when generating hypotheses for experimental validation. However, commonly used methods for generating GWA gene scores are computationally inefficient, biased by gene length, imprecise, or have low true positive rate (TPR) at low false positive rates (FPR), leading to erroneous hypotheses for functional validation. Here we introduce a new method, PEGASUS, for analytically calculating gene scores. PEGASUS produces gene scores with as much as 10 orders of magnitude higher numerical precision than competing methods. In simulation, PEGASUS outperforms existing methods, achieving up to 30% higher TPR when the FPR is fixed at 1%. We use gene scores from PEGASUS as input to HotNet2 to identify networks of interacting genes associated with multiple complex diseases and traits; this is the first application of HotNet2 to common variation. In ulcerative colitis and waist–hip ratio, we discover networks that include genes previously associated with these phenotypes, as well as novel candidate genes. In contrast, existing methods fail to identify these networks. We also identify networks for attention-deficit/hyperactivity disorder, in which GWA studies have yet to identify any significant SNPs.

KEYWORDS GWAS; common variants; complex diseases; pathway analysis; quantitative traits

Genome-wide association (GWA) studies and meta-analyses are widely used to identify susceptibility loci for complex diseases and traits, which are phenotypes generated by multiple mutations of moderate to small effect (Hirschhorn and Daly 2005; McCarthy et al. 2008; Daly 2010; Jiang et al. 2012; Evangelou and Ioannidis 2013; Nalls et al. 2014; Skibola et al. 2014; Woo et al. 2014; Buch et al. 2015; Kouri et al. 2015; Litchfield et al. 2015; Renton et al. 2015; Hallberg et al. 2016). To date, >2400 GWA studies have been conducted to find causal variants that are statistically associated with a disease or trait (http://www.ebi.ac.uk/gwas/). The GWA framework tests the hypothesis that individual mutations of large effect generate phenotypes of interest. However, this framework has multiple limitations when applied to complex diseases. First, complex diseases are known to exhibit genetic heterogeneity on multiple levels: (i) The disease may be generated by multiple mutations within an associated gene and (ii) mutations in distinct genes within a pathway may interact and produce the disease state (McClellan and King 2010). In both cases, separately testing individual variants for statistical associations with a phenotype may not identify susceptibility loci (McClellan and King 2010; Stranger et al. 2011). Further, SNP-level GWA results are unlikely to reveal complex disease mechanisms, given that different combinations of functionally related variants in genes and pathways may interact to produce the phenotype of interest.

Gene-set analyses, which test for the statistical association of phenotype state with a set of genes, are commonly used to address these limitations of the GWA framework (see Wang...
et al. 2010, Leiserson et al. 2013, and Mooney et al. 2014 for reviews). To increase computational efficiency and limit the number of hypotheses tested, it is necessary to reduce the combinations of variants examined to a tractable number. This is typically done using databases of known pathways or other biological interactions, nearly all of which are annotated at the gene level. Thus, a crucial step in most gene-set analyses is combining SNP-level GWA P-values within genes into a “gene score” (Mooney et al. 2014). Here we use “gene-set analysis” to describe three types of statistical tests for association at the gene level with a phenotype of interest. First, we describe permutation tests (e.g., DAPPLE and dmGWAS) (Jia et al. 2011; Rossin et al. 2011) where P-values are assigned to gene scores observed in an annotated pathway. Second, we describe tests for enrichment in related annotations among genes in a predetermined list (e.g., GRAIL, MAGENTA, DAVID, and GSEA-SNP) (Huang et al. 2007; Holden et al. 2008; Raychaudhuri et al. 2009; Segré et al. 2010). To conduct these tests, the investigator must compute a gene score and, in some cases, determine a threshold for extreme gene scores to generate a list of genes associated with the phenotype of interest. In the third type of test, once a gene score is computed, the investigator can conduct a gene-level association test and/or a gene-network association test, to identify novel combinations of variants that generate a phenotype of interest, due to unknown interactions between genes or uncharacterized cross-talk between pathways.

An informative gene score is a necessary ingredient for accurate gene-set analyses, but all commonly used methods for generating gene scores have substantial drawbacks. Commonly used methods include choosing the best SNP P-value within a gene to be the gene score, which is sometimes referred to as “minSNP” (Torkamani et al. 2008; Fehringer et al. 2012; Gelehrter et al. 2015; Hu et al. 2015); permutation-based methods such as permSNP (Wang et al. 2007; Elefterohorinou et al. 2009; Ballard et al. 2010; Christoforou et al. 2014; Evangelou et al. 2014; Backes et al. 2016); regression-based methods such as the sequence kernel association test (SKAT) family of tests (Wu et al. 2010, 2011) and stratified LD score regression (Finucane et al. 2015); and VEGAS (Liu et al. 2010) and RAREMETALS (Liu et al. 2013), which correct for linkage disequilibrium (LD) between SNPs, using simulations from a multivariate normal distribution whose variance is the empirical LD observed among SNPs within each gene being analyzed. Multiple methods exist that use the same null distribution as VEGAS (Tzeng and Zhang 2007; Pan 2009). Other methods that have been proposed include Fisher’s combination test (where the gene score must be calculated empirically using permutation tests), Simes’ combination test, and Sidak’s combination test (Ballard et al. 2010; Peng et al. 2010; Wojcik et al. 2015).

The limitations of these approaches range from biased results to computational inefficiency to imprecision (Table 1). minSNP is heavily biased by gene length; the longer the gene is, the more likely it is to have a low gene score. permSNP permutes case–control labels within a genotype data set to calculate an empirical P-value for every gene, which becomes computationally intractable for large data sets (Liu et al. 2010). Further, permSNP and SKAT require gaining access to genotype data to perform permutations and regression, respectively. The VEGAS method is more computationally efficient than other permutation methods (e.g., permSNP requires recomputing GWA P-values for each permuted data set) and requires only GWA SNP-level P-values as input, but both permSNP and VEGAS give gene scores whose numerical precision depends on the number of permutations and simulations, respectively, that are performed. The smallest gene score VEGAS reports by default is 10^-6 and for permSNP, it is the reciprocal of the number of permutations performed per gene (Table 1).

Here we propose a new method—the precise, efficient gene association score using SNPs (PEGASUS)—to calculate gene scores analytically from a null chi-square distribution that captures LD between SNPs in a gene and addresses the shortcomings of existing methods. PEGASUS requires only GWA study summary statistics and a suitable reference population for LD calculations as input and thus can be applied to GWA study meta-analyses performed on summary statistics, pooled DNA sequencing GWA studies, family-based GWA studies, transmission disequilibrium test (TDT) results, and also traditional GWA studies where consent guidelines prohibit release of genotype data. PEGASUS gene scores are correlated with statistics like VEGAS (Tzeng and Zhang 2007; Pan 2009; Liu et al. 2010), which rely on the same null distributions to calculate gene scores. These methods use different approximations for the distribution of the sum of correlated chi-square statistics, in contrast to the more accurate numerical integration of the null distribution implemented in PEGASUS. We apply our method to publicly available GWA data sets for nine common diseases and three quantitative traits from the Psychiatric Genomics Consortium (PGC) (Neale et al. 2010; Ripke et al. 2011, 2013; Sklar et al. 2011), the International IBID Genetics Consortium (IIBDGC) (Franke et al. 2010; Anderson et al. 2011), the Genetic Investigation of Anthropometric Traits (GIANT) Consortium (Heid et al. 2010; Lango Allen et al. 2010; Speioltes et al. 2010), the Broad Institute (Stahl et al. 2010), the Diabetes Genetics Replication and Meta-analysis (DIAGRAM) Consortium (Morris et al. 2012), and Xu et al. (2013) (Table 2). These data sets were chosen because the full set of SNP-level P-values from the GWA study were available for public download. We compare our method to gene scores generated by minSNP, permSNP, SKAT, and VEGAS, using real and simulated GWA data. Finally, we use our gene scores as input in pathway analysis with HotNet2 (Leiserson et al. 2015), thereby conducting the first application of HotNet2 to common genetic variation and identifying gene networks harboring several variants associated with three phenotypes: attention-deficit/hyperactivity disorder, ulcerative colitis, and waist–hip ratio. For these three phenotypes of interest, HotNet2 using VEGAS gene scores recovered fewer significant subnetworks for attention-deficit/hyperactivity disorder, ulcerative colitis, and waist–hip ratio. Neither VEGAS nor PEGASUS yielded significant subnetworks for the other nine traits studied here.
Materials and Methods

Data sets analyzed from genome-wide association studies

Methods for computing gene scores require a full list of GWA SNP-level P-values; these can be computed from genotype data obtained from previously published GWA studies. We were able to obtain complete results from previous GWA studies for nine common diseases and three quantitative traits (Table 2). See Supplemental Material, Table S3 for URLs to download GWA P-values from the studies referenced in Table 2.

Gene scores

We compared PEGASUS to four existing methods for generating gene-based scores from GWA SNP-level P-values: (i) minSNP (Torkamani et al. 2008; Fehringer et al. 2012; Gelernter et al. 2015; Hu et al. 2015), (ii) permSNP (Wang et al. 2007; Eleftherohorinou et al. 2009; Ballard et al. 2010; Christoforou et al. 2014; Evangelou et al. 2014; Backes et al. 2016), (iii) SKAT (Wu et al. 2010, 2011), and (iv) VEGAS (Liu et al. 2010). For minSNP, the gene scores are the smallest SNP P-value within a given gene set. For permSNP, the gene scores are generated by permuting phenotype labels within a data set, recomputing SNP P-values using the permuted data each time, and selecting the smallest P-value among these permuted P-values. For SKAT, the gene scores are generated by permuting phenotype labels within a genotype data set, recomputing SNP P-values using the permuted data each time, and selecting the smallest P-value among these permuted P-values. For VEGAS, the gene scores are generated by permuting phenotype labels within a genotype data set, recomputing SNP P-values using the permuted data each time, and selecting the smallest P-value among these permuted P-values.

Table 1 Summary of minSNP, permSNP, SKAT, and VEGAS gene score methods and limitations

| Gene score method | How it works | Limitations |
|-------------------|--------------|-------------|
| minSNP            | The gene score for each gene is the smallest SNP P-value observed within that gene in a GWA study. | Biased by gene length (longer genes have lower gene scores). |
| permSNP           | Permutes case–control labels within a genotype data set, recomputes GWA SNP P-values using a permuted data set, and calculates an empirical gene P-value based on the number of times the observed average SNP P-value is lower than the permuted P-values. | Requires access to genotype data; very computationally costly for genome-wide data sets; numerical precision of gene scores is bounded by the number of permutations performed. |
| SKAT              | Uses multiple linear/logistic mixed-model regression of covariates (such as principal components to control for population stratification) and genotypes for variants in a gene set onto disease state. | Requires access to genotype data. |
| VEGAS             | Uses simulations from a multivariate normal distribution to correct for LD between SNPs. The variance of the distribution is the empirical LD observed among SNPs within each gene in the data set. | Numerical precision of gene scores is bounded by the number of simulations performed; computationally inefficient due to simulations. |

SKAT (Wu et al. 2010, 2011): This method uses multiple linear/logistic mixed-model regression of covariates and genotypes for variants in a gene set, along with covariates, onto disease state. Covariates can include sex, age, or top principal components of genotype data to control for population stratification. Under the multiple logistic regression model for a continuous phenotype, the relationship between variant genotypes G_i and the phenotype y_i for the ith individual (of n total individuals) is given by Equation 2, where α_0 is an intercept term, C_i is a vector of covariates, α is the vector of regression coefficients for m covariates, β is the vector of regression coefficients for the n SNPs in a gene, and ε_i is an error term that is normally distributed with mean of zero and variance σ^2. Given this model, SKAT tests the null hypothesis that each gene has a P-value for every gene. We carried out permSNP only on the acute lymphoblastic leukemia (ALL) data set (Xu et al. 2013), as genotype data are required for this method, and we did not have genotype data for the other traits analyzed here. We calculated permSNP gene scores only for the top 400 most significant genes determined by minSNP using set-based test analysis in PLINK due to computational constraints (Purcell et al. 2007) (see File S1, Algorithm S1 for more details.)

The following settings were used to calculate permSNP gene scores in PLINK (Purcell et al. 2007): --set-r2 1, --set-p 1, --set-max 99999, --maf 0.01, and --mperm 10,000 permutations of case–control labels. With these command flags, PLINK first does an association test between phenotype state and allele dosage at each SNP. Second, for every gene, the SNP test statistics (q_1, q_2, ..., q_n) within the gene are averaged to calculate the observed gene-level test statistic Q_\text{obs} (File S1, Algorithm S1). Third, the phenotype labels are permuted M times and the previous two steps are repeated for the permuted data each time, resulting in SNP statistics using the permuted phenotype data and corresponding gene statistics Q^*. The gene score p_g is then the fraction of times the gene statistic Q^* is greater than the observed statistic Q_\text{obs} over the M permutations (File S1, Algorithm S1).
where $K$ is the variance component statistic for this test is given by Equation 3,
and $\text{variance component}$ and $\text{variance}$ for genetic similarity between two subjects $P$ using numerical integration to obtain a $\text{beta distribution density function}$ with parameters $\alpha = 1$ and $\beta = 25$ evaluated at the sample minor-allele frequency (MAF) for a given variant $m$. The SKAT test statistic follows a quadratic form in the random variables $x_i$ and $\epsilon_i$ as follows: Let

$$
\begin{align*}
y_i &= \alpha_0 + \alpha' C_i + \beta' G_{ij} + \epsilon_i \\
Q &= (y - \mu)' K (y - \mu).
\end{align*}
$$

Because full genotype data are required for this method, we applied SKAT only on the ALL data set (Xu et al. 2013) and the Wellcome Trust Case Control Consortium (WTCCC) type 2 diabetes data set (WTCCC 2007). We used the top four principal components from principal components analysis (PCA) on these data sets as covariates in the regression and hold these covariates constant across all methods tested in this study (Wu et al. 2010, 2011; Peloso et al. 2014). The following settings were used to calculate SKAT scores in R, using the R package SKAT (Lee et al. 2015): (a) in the R function SKAT Null Model, out type = “D” and Adjustment = “Fm” and (b) in the R function SKATBinary.SSD.All, method = “SKAT”. These settings specify a linear weighted kernel with the weights $w_i = \text{Beta} \left( \text{MAF}_i; 1, 25 \right)$.

**VEGAS (Liu et al. 2010):** Consider a gene with $n$ SNPs. Under the null hypothesis of no association, a gene can be represented by an $n$-element multivariate normal vector with mean $\mu = 0$ and positive definite covariance matrix $\sum$, where $\sum_{ij}$ is the LD between SNP $i$ and SNP $j$ and $\sum_{ii} = 1$. The quadratic form in the random variables $X_1, X_2, \ldots, X_n$ associated with an $n \times n$ symmetric matrix $A = (a_{ij})$ is defined as $Q(X) = Q(X_1, X_2, \ldots, X_n) = X'AX = \sum_{i=1}^{n} \sum_{j=1}^{n} a_{ij} X_i X_j$ (Mathai and Provost 1992). The quadratic form $Q(X) = X'AX$ has the following representation (Equation 5), where $\lambda$ are the eigenvalues of $\sum \text{and}$ $U$ are mutually independent standard normal variables (Mathai and Provost 1992):

$$Q(X) = \sum_{i=1}^{n} \lambda_i U_i^2.$$  

$$Q \text{ of } \sum_{i=1}^{n} X_i^2 \text{ follows the same distribution as Equation 5, and so the characteristic function of } Q(X) \text{ can be inverted to find the CDF of the null distribution.}$$
The numerical integration is implemented in the R package CompQuadForm (Duchesne and Lafaye De Micheaux 2010). The LD (covariance) matrix $S$ is calculated using the --r flag (correlation) in PLINK (Purcell et al. 2007). In contrast, VEGAS (Liu et al. 2010) draws samples from the multivariate normal distribution with variance equal to the LD matrix, which are then summed to obtain an approximation of the $P$-value. Software to run PEGASUS is available at https://github.com/ramachandran-lab/PEGASUS. Empirical LD can be calculated using the 1000 Genomes Phase 3 data set (Auton et al. 2015) (release date: November 2014) as references. These data contain 2426 individuals in five superpopulations: East Asians, Europeans, Africans, South Asians, and admixed Americans.

Connection between SKAT and PEGASUS tests: As shown in Text S1, the SKAT and PEGASUS null distributions are mixtures of chi-square distributions. Mixture proportions for the SKAT null distribution are the eigenvalues of the matrix $\sigma^2((1-P)K)$, where $P = C(C^T C)^{-1}C^T$ is a projection matrix dependent on the covariate matrix $C$ and $K = GWG'$ is a kernel matrix dependent on the genotype matrix $G$ and a diagonal matrix of weights $W$. For the PEGASUS null distribution, mixture proportions are given by the eigenvalues of the LD matrix $\sum$. If no covariates are considered and the variant weights are uniform ($w_j = 1$) for all variants, the SKAT null distribution becomes a mixture of chi-square distributions with mixture proportions given by the eigenvalues of the $K = GWG'$ matrix, which is a variance–covariance matrix similar to the PEGASUS LD matrix $\sum$. Thus, under these circumstances, the two tests give similar results. However, PEGASUS requires only summary statistics and is a better choice when genotype data are not available for analysis.
**GWA study replication**

To further assess the robustness of our method, PEGASUS, we attempted to replicate gene hits ($p < 2.8 \times 10^{-6}$ or 0.05 divided by approximately 18,000 genes tested) generated by PEGASUS for four data sets [bipolar disorder (BIP), Crohn’s disease (CD), rheumatoid arthritis (RA), and type 2 diabetes (T2D)], using genotype data from the WTCCC (WTCCC 2007). For the replication study, we carried out PEGASUS on these four WTCCC data sets (our “replication cohort”) and compared the top genes found in our “discovery” data sets (Franke et al. 2010; Stahl et al. 2010; Sklar et al. 2011; Morris et al. 2012) to those found in the WTCCC data sets. We note that this is not an independent replication study since the WTCCC data sets were included in the discovery cohorts; cases from the WTCCC data sets comprised at most 38% of the cases included in the discovery cohorts (Table S2). The replication data sets consist of ~2000 cases for each disease and ~3000 shared controls recruited from the United Kingdom and genotyped on the Affymetrix 500K GeneChip (WTCCC 2007).

Eight quality control steps were carried out for each of the four WTCCC data sets. Steps 1–7 were carried out using PLINK (Purcell et al. 2007) (version 1.07):

1. Markers with minor allele frequency <1% were removed.
2. Loci with a call rate ≤95% across individuals were removed.
3. Individuals with at least 5% missingness across all loci were removed.
4. Loci not in Hardy–Weinberg equilibrium were removed ($P$-value threshold of $10^{-5}$).
5. Individuals were pruned based on inbreeding coefficient ($F = 0.05$ or $F = -0.025$).
6. Duplicate individuals were removed (one individual for each pair with identity by state ≥95%).
7. Related individuals were removed (one individual for each pair with $\rho > 0.0175$).
8. Individuals determined to be outliers by principal component analysis were removed. SmartPCA from the EIGENSOFT (Price et al. 2006) software package (version 4.0.2) was used to do PCA with outlier removal. Five iterations of outlier removal were performed with the outlier $\sigma$ threshold = 6.

We conducted GWA analysis using PLINK (Purcell et al. 2007) (version 1.07) on the WTCCC data sets. SNP-level $P$-values were determined by logistic regression of disease state onto minor allele dosage, using the top four principal components as covariates in the logistic regression to control for ancestry.

**GWA study simulation**

To compare how well minSNP, SKAT, VEGAS, and PEGASUS can recover causal genes, we conducted a GWA study for a simulated complex phenotype with known genetic architecture based on the approach outlined in Wojcik et al. (2015) and applied these four methods to the simulated data (Figure S13). To choose causal genes, we picked four pathways with >20 genes each at random from the KEGG pathway database (Kanehisa 1997; Kanehisa et al. 2012). For each pathway, we randomly sampled 20% of its genes, resulting in 54 total causal genes. We ran Tagger (Haploview, Version 4.3) (Barrett et al. 2005) on each gene to find independent tag SNPs ($r^2 < 0.2$), using the WTCCC controls ($N = 2900$ individuals) as reference individuals to calculate LD. For each of the 54 causal genes, we chose 1, 2, or 5 tag SNPs to be associated with the phenotype, giving 123 total causal SNPs. All the chosen SNPs in each gene were randomly assigned an effect size of either 1.2 or 2 to simulate a range of effect sizes.

Using software from Wojcik et al. (2015), we then calculated a per-individual liability score for each individual (WTCCC controls served as our simulated cases and controls) from a model of additive genetic effects by summing the effect size $s$ of each SNP multiplied by the minor allele dosage $X$ at the SNP over all $n$ SNPs (Equation 6). A “wiggle” ($\epsilon$) was added to each raw liability score (Equation 7) to allow the cases and controls to overlap in their liability score distributions:

$$\text{raw liability score} = \sum_{i=1}^{123} s_i X_i$$

$$\text{wiggled score} = \text{raw liability score} + \epsilon,$$

where $\epsilon \sim N(0.1, 10)$.

Phenotype was assigned to each individual based on the mean of 100 deviates from the binomial distribution with probability of success equal to the probability of the wiggled score from the logistic distribution, which we obtained by applying the logistic function to the wiggled score.

We then conducted GWA analysis using PLINK (Purcell et al. 2007) (version 1.07) on the WTCCC controls and the simulated phenotypes. SNP-level $P$-values were determined by logistic regression of minor allele dosage onto disease state. We used the top four principal components, determined by applying smartPCA (Price et al. 2006) to the genotypes, as covariates in the logistic regression to control for ancestry. To simulate spurious associations between SNPs and our associated phenotype, we added 20% of significant SNP $P$-values (144 new SNPs total) from an existing GWA study on CD (Franke et al. 2010) to our simulated GWA $P$-values; these spuriously associated SNPs did not overlap with SNPs already associated with simulated phenotype. By “spuriously associated” SNPs, we mean SNPs that achieve genome-wide significance ($P$-value < $5 \times 10^{-8}$) but are not discussed or selected for replication studies, eQTL analysis, or other downstream analyses due to filtering steps. Such SNPs may be excluded based on criteria such as failure to achieve significance within a majority of the individual cohorts analyzed in a meta-analysis (Anderson et al. 2011), location within regions with complex LD or complex association patterns with the trait such as the MHC or TNFAIP3...
regions for RA (Stahl et al. 2010), or \( P \)-value thresholds based on additional in silico analyses such as GRAIL (Raychaudhuri et al. 2009; Franke et al. 2010). Since the true causal genes underlying the simulated phenotype are known, we are able to measure true positive rate (TPR) and false positive rate (FPR) for each gene score method and used the following gene score thresholds: \( 7.5 \times 10^{-1}, 5 \times 10^{-1}, 2.5 \times 10^{-1}, 10^{-1}, 7.5 \times 10^{-2}, 5 \times 10^{-2}, 2.5 \times 10^{-2}, 10^{-2}, \ldots, 7.5 \times 10^{-16}, 5 \times 10^{-16}, 2.5 \times 10^{-16} \) We find that our simulation results are robust to varying percentages of spurious associated SNPs added and the GWA data set used (Figure S14).

**Pathway analysis**

We performed pathway analysis with HotNet2 (Leiserson et al. 2015), a topology-based method for finding significantly mutated subnetworks within protein–protein interaction networks, originally developed for analyzing somatic mutation data from cancer data sets. HotNet2 uses directed heat diffusion along interaction networks where every gene, represented by nodes in the network graph, has a “heat score” based on its gene score. We used negative log-transformed gene scores generated by PEGASUS, VEGAS, and minSNP as heat scores in HotNet2.

We use HotNet2 to find gene interaction subnetworks containing genes that we have highest confidence are truly associated with the phenotype. We found that HotNet2 does not perform well when too many genes are assigned similar heat scores, as will happen when the majority of genes have insignificant \( P \)-values. Thus, following the approach used in earlier applications of HotNet2 to somatic mutations in cancer, we assigned heat scores of zero to genes that we have previously associated SNPs added and the GWA data set used (Figure S14).

**Data availability**

GWA \( P \)-values analyzed here (Table 2) can be accessed at the URLs given in Table S3. WTCCC data (WTCCC 2007) used in power simulations and replication studies can be accessed through the Wellcome Trust Case Control Consortium: http://www.wtccc.org.uk/. PEGASUS software and LD reference data are available online at the following URL: https://github.com/ramachandran-lab/PEGASUS. HotNet2 (Leiserson et al. 2015) software is available online at the following URL: https://github.com/raphael-group/hotnet2.

**Results**

**Performance comparison of PEGASUS against minSNP, permSNP, SKAT, and VEGAS**

We compared PEGASUS against minSNP (Torkamani et al. 2008; Fehring et al. 2012; Gelernter et al. 2015; Hu et al. 2015), permSNP (Wang et al. 2007; Eleftherohorinou et al. 2009; Ballard et al. 2010; Christoforou et al. 2014; Evangelou et al. 2014; Backes et al. 2016), SKAT (Wu et al. 2010, 2011), and VEGAS (Liu et al. 2010) (Figure 2 and Figure S15), using several metrics to evaluate the different scores.

We find that, for all 12 GWA data sets analyzed, minSNP gene scores are almost always smaller than PEGASUS gene scores (Figure 2A and Figure S1). We also find that minSNP gene scores show a clear dependence on gene length; as the number of SNPs in a gene increases, the minSNP gene score decreases for all data sets analyzed. In contrast, PEGASUS gene scores do not show this trend (Figure 2A, Figure S2, and Figure S16).

We tested whether two corrections to minSNP gene scores mitigated its bias with gene length: (i) calculating \( P \)-values for minSNP gene scores from the Beta(1, \( n \), \( n \) of SNPs in gene) distribution (note that minSNP can be thought of as the first-order statistic for SNP \( P \)-values) and (ii) multiplying minSNP gene scores by the number of SNPs in a gene. Both corrections resulted in gene scores that decrease with increasing gene length (Figure S7 and Figure S8).

Since permSNP requires genotype data and is computationally expensive, permSNP was carried out only on the ALL data set (Xu et al. 2013), using 10,000 permutations; thus, there is large variation in PEGASUS gene scores at a
permSNP gene score of $10^{-4}$ (Figure 2B). Further, permSNP is extremely computationally costly: Carrying out permSNP on a random subset of 400 genes took ~6 hr. Thus, permSNP would be extremely computationally inefficient for analyzing a genome-wide human data set (~18,000–20,000 genes).

Since SKAT requires genotype data, SKAT was carried out on the ALL (Xu et al. 2013) and the WTCCC T2D (WTCCC 2007) data sets, using the top four principal components from PCA on these data sets as covariates. We find that PEGASUS gene scores and SKAT gene scores are correlated ($r = 0.44$ and $r = 0.49$; $P$-values $< 2 \times 10^{-16}$ and $< 2 \times 10^{-16}$ for ALL and T2D, respectively) for both data sets (Figure S15, A and B). We also find that PEGASUS gene scores and unweighted SKAT gene scores are correlated ($r = 0.96$ and $r = 0.94$; $P$-values $< 2 \times 10^{-16}$ and $< 2 \times 10^{-16}$ for ALL and T2D, respectively) (Figure S15, C and D).

Compared to VEGAS, our method has increased numerical precision when calculating gene scores (Figure 2C). Due to its underlying Monte Carlo simulations ($10^9$ by default), VEGAS does not calculate gene scores less than the reciprocal of the number of simulations. However, PEGASUS can evaluate gene scores to the machine precision of R, which is $\approx 10^{-16}$. In addition, VEGAS gene scores become inaccurate close to $10^{-6}$ due to the random nature of Monte Carlo simulations (Figure 2C), whereas PEGASUS does not have a stochastic element. We find that VEGAS produces less numerically precise gene scores than PEGASUS in all 12 data sets analyzed (Figure S3). We also find that PEGASUS runs twice as fast as VEGAS when using HapMap data (Frazer et al. 2007) (Phase 2) as references for LD.

**Enrichment for known associations in real data**

To assess how well minSNP and PEGASUS recover known GWA associations, we calculated the percentage of genes with significant minSNP and PEGASUS gene scores ($P_g < 2.8 \times 10^{-6}$) for the 12 phenotypes in this analysis that have been found to be significantly associated (SNP-level $P$-value $< 5 \times 10^{-8}$) with the disease or trait in GWA studies conducted with different genotype data (Figure 3). Taking known associations to be “true positives,” we calculated positive predictive values (PPV) for every gene score for every disease. We find that in 10 of 12 data sets, significantly associated PEGASUS gene hits ($P_g < 2.8 \times 10^{-6}$) have higher PPV than minSNP gene hits by as much as 2.8-fold, showing that PEGASUS gene hits are enriched for known associations in comparison to minSNP (Figure 3). For the remaining two disorders, attention-deficit/hyperactivity disorder (ADHD) and major depressive disorder (MDD), minSNP identifies significantly associated genes ($P_g < 2.8 \times 10^{-6}$) that have not been found in other GWA studies while PEGASUS does not report any findings (Figure 3).

**Replication of PEGASUS gene hits in WTCCC data**

We attempted to replicate gene hits ($P_g < 2.8 \times 10^{-6}$) generated by PEGASUS for four data sets (BIP, CD, RA, and T2D) for which we have genotype data from the WTCCC (WTCCC 2007). We note that our replication cohorts (WTCCC) were included in the discovery cohorts, and thus this is not an independent replication. We find that we are able to replicate up to 57.2% of gene hits in the case of RA and as low as 0 gene hits in the BIP data set (Table S2). We note that the four meta-analyses we consider our “discovery cohorts” are

**Figure 2** Quantile-quantile plots comparing gene scores produced by PEGASUS against those produced by minSNP, permSNP, and VEGAS. (A) Quantile-quantile plots of PEGASUS gene scores vs. minSNP gene scores. Each point represents a gene and is colored yellow, red, or blue based on gene length percentile, 0–25%, 25–75%, and 75–100%, respectively. The phenotype used is waist–hip ratio (WHR). minSNP gene scores are smaller than PEGASUS gene scores and decrease with increasing number of SNPs in a gene. The deviations from $y = x$ show that minSNP scores are biased toward being smaller than PEGASUS scores, and this bias increases for increasing gene length (genes colored in blue and red). (B) Base-10 logarithm of PEGASUS gene scores vs. base-10 logarithm of permSNP gene scores for acute lymphoblastic leukemia (ALL). permSNP can determine gene scores only as low as the reciprocal of the number of permutations (10,000 in this case) whereas PEGASUS can determine gene scores as low as $2.22 \times 10^{-16}$ (the numerical precision of R). Note that the minimum permSNP scores of $10^{-6}$ differ widely from their $P$-values computed by PEGASUS. (C) Base-10 logarithm of PEGASUS gene scores vs. base-10 logarithm VEGAS gene scores. Using 1 million simulations, the lowest gene scores output by VEGAS are $10^{-6}$, while PEGASUS determines gene scores as low as $2.22 \times 10^{-16}$. In addition, for gene scores close to the reciprocal of the maximum number of simulations performed, VEGAS can return inaccurate gene scores compared to PEGASUS.
composed of much larger sample sizes than our replication data sets and thus had greater power to identify associated variants. Further, we do not necessarily follow the same steps for quality control and ancestry correction in our GWA study as did the meta-analyses reanalyzed here (see Materials and Methods), which may explain our low percentage of replicated significant genes for BIP and CD.

**Power analysis using simulated GWA data**

To compare how well minSNP, SKAT, VEGAS, and PEGASUS can recover causal genes, we conducted gene-level tests for association, using these methods on a GWA study for a simulated phenotype calculated from a model of additive genetic effects. PEGASUS and VEGAS outperform minSNP with a 30% TPR when the FPR is fixed at 1%, and PEGASUS and VEGAS outperform SKAT with 28% higher TPR when FPR is fixed at 1% (Figure 4). We find that minSNP, when applied to the GWA data sets in Table 2, outputs high numbers of significant genes (genes with \(p < 2.8 \times 10^{-6}\)). For example, as many as 5.5% of all genes (lower bound: 0.01%) are below the Bonferroni-corrected threshold for significance when using minSNP across the 12 data sets we analyzed (Table S1). In our simulation, we find that the high FPR in minSNP is due to genes with spurious SNP association P-values added in as part of the simulation. This suggests that some minSNP gene hits in observed GWA studies are spurious associations as well. By correcting for LD, PEGASUS and VEGAS are able to ignore these false positives (Figure 4). At very low FPR (\(< 0.34\%\)), SKAT is the most sensitive method, but SKAT has lower sensitivity overall. This could be a desirable feature if one is looking for a small number of reliable gene hits. However, for pathway/network analysis, it is useful to obtain high sensitivity, as the pathway/network information will help reduce the remaining false positives. We were unable to add in spurious SNP association P-values for the SKAT method since this test requires genotype data; however, inclusion of these SNPs could only decrease the performance of SKAT in simulation.

**The downstream effect of gene scores on pathway analysis**

Using gene scores generated from minSNP, VEGAS, and PEGASUS as input to HotNet2 (Leiserson et al. 2015), we performed pathway analysis on each of the 12 GWA data sets. We find significantly associated gene subnetworks for ADHD, ulcerative colitis (UC), and waist–hip ratio adjusted for body mass index (WHR). Figure 5 shows a selection of subnetworks containing known or biologically plausible gene associations for these three phenotypes based on previous GWA or functionalstudies. Other significantly associated subnetworks can be found in Figure S9 and Figure S12. PEGASUS identifies multiple subnetworks containing genes with known associations to each phenotype of interest. Some of these subnetworks are not found when using minSNP and VEGAS gene scores as input to HotNet2 (Figure S10 and Figure S11). We also identify subnetworks associated with ADHD (Figure 5, D–F), a disorder for which GWA studies have not identified any SNPs with genome-wide significance. We detail our findings for each disease or trait below.
UC: Inflammatory bowel disease (IBD), an inflammatory disease of the gastrointestinal tract, has two major subtypes: UC and CD. IBD is hypothesized to result from dysregulated T-cell immune responses to commensal enteric bacteria in the gut that develop in individuals who are genetically predisposed to the disease. Environmental factors also play an important role in triggering onset or recurrence of symptoms (Sartor 2006; Lee et al. 2012). UC is characterized by superficial, ulcerating inflammation that is limited to the colon (Christophi et al. 2012).

HotNet2 analysis using PEGASUS scores identifies a subnetwork containing several genes in JAK2-STAT signaling pathways as associated with UC disease state (Figure 5A). The subnetwork in Figure 5A contains the genes JAK2, IL12RB2, IFNG, PTPN2, and STAT4, which all have genome-wide significant SNP hits (SNP P-value < 5 \times 10^{-8}) in GWA studies for IBD (Duerr et al. 2006; Jostins et al. 2012). The gene IFNG also has genome-wide significant SNPs in GWA studies for ulcerative colitis conducted with different data sets from the data set used in this study (2.5 \times 10^{-12} and 4.2 \times 10^{-12}) (Silverberg et al. 2009; McGovern et al. 2010). The following genes shown in this subnetwork have also been significantly associated (SNP P-value < 5 \times 10^{-8}) with CD (CD alone or in concert with psoriasis or celiac disease) in other GWA studies: JAK2, IL12RB2, SOCS1, and PTPN2 (Raelson et al. 2007; WTCCC 2007; Barrett et al. 2008; Franke et al. 2010; Festen et al. 2011; Ellinghaus et al. 2012). Two closely related pro-inflammatory cytokine signaling pathways involve many genes shown in this subnetwork: the interleukin (IL)-23/type 17 helper T-cell (T_{H17}) signaling pathway and the IL-12/type 1 helper T-cell (T_{H1}) signaling pathway. Both signaling pathways ultimately result in cytokine-mediated gut destruction (Wang et al. 2010; Parkes et al. 2013).

Similar pathways centered around IL-12, IL-23, and JAK2-STAT signaling have been manually compiled based on GWA studies for CD and IBD (Wang et al. 2010; Parkes et al. 2013). In addition, the subnetwork (Figure 5A) contains the gene PTPN2, which encodes protein tyrosine phosphatase nonreceptor type 2 (PTPN2) and has been shown to regulate autophagy in human intestinal epithelial cells; knockdown of PTPN2 caused impaired autophagosome formation and dysfunctional autophagy that eventually resulted in increased apoptosis of intestinal cells in response to IFNG and tumor necrosis factor-α (Scharl et al. 2012). This subnetwork illustrates interactions between multiple genes involved in the immune response to pathogens that may underlie the pathology of ulcerative colitis.

The subnetwork we identify in Figure 5B shows interactions between the human leukocyte antigen (HLA) class I genes and transporter associated with antigen processing (TAP) genes. These genes are thought to underlie IBD pathology as well as other immune-mediated disorders such as psoriasis and ankylosing spondylitis (Parkes et al. 2013). Finally, HotNet2 reports a significantly associated subnetwork containing genes that are part of the tumor necrosis factor (TNF) signaling pathway (Figure 5C). TNF signaling results in activation of nuclear factor kappa-light-chain enhancer of activated B cells (NF-κB), which is a known inflammatory response in IBD (Anderson et al. 2011). Additional significant gene subnetworks are shown in Figure S12.

We emphasize that neither the JAK2-STAT subnetwork (Figure 5A) nor the HLA class 1 and TAP genes (Figure 5B) are found when using VEGAS gene scores as input to HotNet2 (Figure S11), demonstrating the importance of high-precision gene scores in downstream analysis.

ADHD: ADHD is a highly heritable neuropsychiatric disorder characterized by the following traits: inattention, hyperactivity, and impulsivity (Franke et al. 2009). It is thought to be a very complex multifactorial trait and, despite high heritability estimates (76%) (Neale et al. 2010), it has been difficult to find genes underlying the phenotype. GWA studies with very large sample sizes have been performed, yet no variants have reached genome-wide significance (Franke et al. 2009).

Using PEGASUS gene scores as input to HotNet2, we find five significantly associated gene subnetworks associated with ADHD (Figure 5 and Figure S9). Figure 5D includes interactions between multiple genes previously associated with cognition-related traits and neurodevelopmental disorders. RPS6KA5, PDZD2, and RAII are associated with years of education (GWA SNP P-values of 9.2 \times 10^{-4}, 5.9 \times 10^{-4}, and 3.6 \times 10^{-5}, respectively) (Rietveld et al. 2013). The genes RPS6KA5, PDZD2, and ST3GAL3 have also been associated.
The second subnetwork (Figure 5E) contains FURIN and other genes that play important roles in cell trafficking processes that may be involved in the pathology of neuropsychiatric and cognitive disorders such as Alzheimer’s disease and intellectual disability (Wan et al. 1998; Fuentealba et al. 2010; Carlino et al. 2013). A third subnetwork (Figure 5F) contains genes that are likely involved in brain development (Maden 2007). Two additional subnetworks found by HotNet2 using PEGASUS scores contain genes that play regulatory roles in neurogenesis and responses to stress (Figure S9A) and genes associated with other social and behavioral abnormalities (Figure S9B). Additional information about genes in these subnetworks can be found in Text S2.

**WHR adjusted for body mass index:** WHR adjusted for body mass index (BMI) is a quantitative trait that measures body fat distribution. Both WHR and BMI areheritable traits (25–70% heritability), but mechanisms underlying body fat distribution are still unclear (Baker et al. 2005). WHR is a useful trait for predicting risk for T2D and heart disease since it accounts for waist and hip size, which both have associations with these traits (Heid et al. 2010). Increasing waist size is associated with increased risk for T2D and heart disease, but gluteal fat deposits play a protective role against T2D,
hypertension, and dyslipidemia (Heid et al. 2010; Shungin et al. 2015).

HotNet2 analysis with PEGASUS gene scores identifies two subnetworks with interactions between genes known to be associated with WHR that may shed light on the genetic determination of body fat distribution. Figure 5G displays a subnetwork of homeobox (HOX) genes, a family of transcription factors that play an important role in morphogenesis in animals (Zhang et al. 2007). The complete HOX gene network was found to be active in human white adipose tissue and fetal brown adipose tissue (Cantile et al. 2003). HOX genes contained in this subnetwork include HOXA9, HOXC11, HOXA11, and EMX2. Multiple studies of gene expression in human subcutaneous abdominal adipose tissue and gluteal adipose tissue found that the HOXA9 gene has increased expression in abdominal adipose tissue; MEIS1, which encodes a HOX cofactor and is also contained in this subnetwork, was also expressed more in abdominal adipose tissue than in gluteal depots in men only (Karpe and Pinnick 2015). In contrast, HOXC11 and HOXA11 have increased gene expression in gluteal adipose tissue than in abdominal adipose tissue (Karpe and Pinnick 2015). HOXA9 and EMX2, another homeobox gene, were induced after extreme weight loss following bariatric surgery (Tchkonia et al. 2013). The subnetwork shows SOX8, which encodes a transcription factor thought to play a role in development; mice deficient in SOX8 develop surprisingly normally, but undergo a severe degeneration of adipose tissue as adult mice (Guth et al. 2009). Guth et al. (2009) posit that SOX8 plays a role in adipocyte development, especially during replenishment of the adipocyte pool in adult mice. IRF4 is also contained in this subnetwork and encodes interferon regulatory factor 4 (IRF4), which is part of a family of transcription factors that are involved in various immune functions including regulation of innate immunity via the Toll-like receptor (TLR) signaling pathway (Eguchi et al. 2011). Many IRF proteins including IRF4 are also expressed in preadipocytes and mature adipocytes; their function is to repress adipogenesis (Eguchi et al. 2008). Eguchi et al. (2011) find that knockout mice lacking IRF4 in adipocytes display excess adiposity and resistance to lipolysis induced by catecholamines, fasting, or cold exposure, suggesting that IRF4 plays an important role in transcriptional regulation of lipid handling in fat. These findings indicate that this subnetwork may play an important role in development of adipocytes and fat distribution.

The second subnetwork found by HotNet2 (Figure 5H) elucidates the interactions of VEGFA, which contains a known GWA study association for WHR (SNP P-value $1.38 \times 10^{-10}$) and VEGFB, which is moderately associated with WHR (SNP P-value $7.2 \times 10^{-5}$) (Heid et al. 2010). Additional information about this subnetwork can be found in Text S3.

We also conducted HotNet2 analysis using minSNP gene scores for all phenotypes studied here. Since minSNP gene scores are misleadingly small (Figure 2A, Figure S2, and Figure S16), single highly significant genes pull in many unrelated genes with low gene scores to create artifactual “star-shaped” subnetworks that are likely false positives (see Figure S10 for HotNet2 results using minSNP gene scores for ulcerative colitis).

**Discussion**

Here we present a new approach for identifying geno-phenotype associations from case–control data that combines a novel gene score, PEGASUS, with network-based analyses using HotNet2 (Leiserson et al. 2015). PEGASUS computes gene scores that measure the statistical association of a gene with a phenotype of interest and has multiple advantages over commonly used methods for generating gene scores.

First, PEGASUS analytically models LD among SNPs within genes, producing a computationally efficient method that yields precise results—gene scores as small as $2.22 \times 10^{-16}$ (the machine precision of R). By modeling linkage disequilibrium, PEGASUS, like VEGAS (Liu et al. 2010), is sensitive to genes with multiple SNPs that are moderately associated with the phenotype of interest. Unlike existing methods, our gene scores are not biased by gene length or poor precision. In the future, our approach can be extended to combine SNP-level P-values within linkage blocks in contrast to the gene boundaries used in this study.

Second, we apply PEGASUS to 12 genome-wide association studies for complex diseases and traits and, in 10 of 12 studies, our significant gene scores ($p_g < 2.8 \times 10^{-6}$) enrich for genes known to be associated with the phenotypes of interest (Figure 3). In simulation studies, we find that modeling fine-scale LD (or pairwise correlations between SNPs within genes), as in the PEGASUS and VEGAS methods, produces gene scores with much higher true positive rates of identifying genes associated with the simulated phenotype than does using minSNP (Figure 4). Thus, PEGASUS can be applied after conducting a GWA study to prioritize genes for functional validation.

Third, because our approach precisely assesses the statistical association of a gene with a phenotype of interest, PEGASUS offers the opportunity to identify novel sets of interacting genes underlying complex phenotypes via pathway or network analysis with our gene scores as input. Complex phenotypes may be generated via mutations in a subset of genes in a predefined gene set [such as the gene sets used in gene set enrichment analysis (Subramanian et al. 2005)] or via crosstalk between gene sets or pathways. To identify novel subnetworks of genes associated with each of the complex phenotypes analyzed in this study, we used gene scores generated by PEGASUS as input to HotNet2 (Leiserson et al. 2015); this is the first application of HotNet2 to common genetic variation. In our network analyses, minSNP and VEGAS miss key subnetworks containing genes known to be associated with the phenotype of interest (Figure 5, A and B, ulcerative colitis).

Fourth, in ADHD, a disease for which large GWA studies ($n > 9543$ individuals) have not identified genome-wide significant associations (Franke et al. 2009; Neale et al. 2010),
we identify significant subnetworks of interacting genes ($p \leq 0.05$) that are involved in neural development and learning and cognition. As knowledge of the human interactome continues to improve, post hoc analysis of GWA studies using gene scores from PEGASUS in conjunction with HotNet2 has the potential to generate promising hypotheses for functional validation.

Finally, we argue that human genetics would benefit greatly if more GWA studies released all SNP-level $P$-values generated, instead of reporting a subset of $P$-values the authors consider to be of interest. The present situation, where only the genotypes are deposited in public repositories under managed access, makes it impossible to replicate the various filtering, quality control, ancestry correction, and other steps that lead from raw genotype calls to the handful of genome-wide significant SNPs reported in publications. Of course, participant confidentiality requirements may limit the public distribution of SNP $P$-values (Masca et al. 2011), but $P$-values could be released with the genotype data under a managed access model. If these summary statistics were routinely released, gene score methods like PEGASUS, network/pathway analyses like HotNet2 (Leiserson et al. 2015), and other computational innovations from the community could be more widely applied to yield new insight into the genomic underpinnings of complex diseases and traits.

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Simulation Part 1 - Choosing causal genes and SNPs:

1. KEGG Pathway Database
   - Choose 4 pathways at random with >20 genes each
   - Randomly sample 20% of genes in each pathway
   - 54 causal genes
   - Run Tagger to find tag SNPs with $r^2 < 0.2$
   - 382 tag SNPs
   - Choose 1, 2, or 5 tag SNPs from each gene
   - 123 causal SNPs
   - Assign all causal SNPs in each gene effect size of 1.2 or 2
   - OR: 1.2, OR: 2

Simulation Part 2 - GWA study on simulated phenotype:

1. Simulated phenotypes for each WTCCC indiv. based on causal SNPs (see Methods)
2. Perform GWAS in PLINK using logistic regression
3. Top 4 PCs from PCA to control for ancestry
4. Genome-wide significant SNPs from real GWA data introduce spurious associations
5. GWAS p-values + spurious associations
6. Perform PEGASUS and minSNP analysis
7. Simulated gene scores
| Disease or Trait | Level of Significance for gene score ($\times 10^{-6}$) | # of significant genes (minSNP) | % significant genes (minSNP) | # of significant genes (PEGASUS) | % significant genes (PEGASUS) | # of significant genes (VEGAS) | % significant genes (VEGAS) |
|-----------------|-------------------------------------------------|--------------------------------|----------------------------|---------------------------------|-------------------------------|-------------------------------|----------------------------|
| ADHD            | 2.81                                            | 1                              | 0.01                       | 0                               | 0                             | 0                             | 0                           |
| (NEALE et al. (2010)) |                                               |                                |                            |                                 |                               |                               |                             |
| ALL             | 2.78                                            | 29                             | 0.16                       | 10                              | 0.06                          | 10                            | 0.06                        |
| (Xu et al. (2013)) |                                               |                                |                            |                                 |                               |                               |                             |
| BIP             | 2.81                                            | 47                             | 0.26                       | 17                              | 0.1                           | 17                            | 0.1                         |
| (SKLAR et al. (2011)) |                                               |                                |                            |                                 |                               |                               |                             |
| BMI             | 2.83                                            | 96                             | 0.54                       | 56                              | 0.32                          | 56                            | 0.32                        |
| (SPELIOTES et al. (2010)) |                                               |                                |                            |                                 |                               |                               |                             |
| CD              | 2.88                                            | 431                            | 2.48                       | 256                             | 1.47                          | 249                           | 1.43                        |
| (FRANKE et al. (2010)) |                                               |                                |                            |                                 |                               |                               |                             |
| Height          | 2.83                                            | 834                            | 4.71                       | 404                             | 2.28                          | 397                           | 2.24                        |
| (LANGO ALLEN et al. (2010)) |                                               |                                |                            |                                 |                               |                               |                             |
| MDD             | 2.81                                            | 16                             | 0.09                       | 0                               | 0                             | 0                             | 0                           |
| (RIPKE et al. (2013)) |                                               |                                |                            |                                 |                               |                               |                             |
| RA              | 2.80                                            | 252                            | 1.41                       | 180                             | 1.01                          | 183                           | 1.03                        |
| (STAHL et al. (2010)) |                                               |                                |                            |                                 |                               |                               |                             |
| SCZ             | 2.81                                            | 250                            | 1.41                       | 55                              | 0.31                          | 55                            | 0.31                        |
| (RIPKE et al. (2011)) |                                               |                                |                            |                                 |                               |                               |                             |
| T2D             | 2.82                                            | 54                             | 0.3                        | 11                              | 0.06                          | 10                            | 0.06                        |
| (MORRIS et al. (2012)) |                                               |                                |                            |                                 |                               |                               |                             |
| UC              | 2.80                                            | 980                            | 5.5                        | 190                             | 1.07                          | 191                           | 1.07                        |
| (ANDERSON et al. (2011)) |                                               |                                |                            |                                 |                               |                               |                             |
| WHR             | 2.83                                            | 50                             | 0.28                       | 17                              | 0.1                           | 18                            | 0.1                         |
| (HEID et al. (2010)) |                                               |                                |                            |                                 |                               |                               |                             |

Number of significant genes and percentage of significant genes (out of the total number of genes considered) for minSNP, PEGASUS and VEGAS gene scores. Significance is based on Bonferroni correction for the total number of genes for which the study had SNP-level $p$-values in each of 12 GWA datasets (Table 2). We find that minSNP always finds more associated genes than the other two methods. PEGASUS and VEGAS typically find similar numbers of associated genes.
| Disease Trait | Reference Data | # WTCCC Cases in Reference Data | # Non-WTCCC Cases in Reference Data | # of PEGASUS Hits in Reference Data replicated in WTCCC data | Total # PEGASUS hits in Reference Data | % PEGASUS hits replicated in WTCCC data (Column 5/Column 6) |
|----------------|----------------|---------------------------------|-------------------------------------|------------------------------------------------------------|--------------------------------------|----------------------------------------------------------|
| BIP            | SKLAR et al. (2011) | 1,571                           | 5,910                               | 0                                                          | 17                                   | 0.0                                                      |
| CD             | FRANKE et al. (2010) | 1,747                           | 4,586                               | 11                                                         | 254                                  | 4.3                                                      |
| RA             | STAHL et al. (2010) | 1,525                           | 4,014                               | 103                                                        | 180                                  | 57.2                                                     |
| T2D            | MORRIS et al. (2012) | 1,924                           | 10,247                              | 1                                                          | 11                                   | 9.1                                                      |

**Replication of PEGASUS gene hits in WTCCC datasets.** We conducted a replication experiment for PEGASUS gene hits for the 12 GWA datasets in this study in WTCCC data for Bipolar Disorder (BIP), Crohn’s Disease (CD), Rheumatoid Arthritis (RA) and Type 2 Diabetes (T2D). A “hit” is a gene with a gene score $p_g < 2.8 \times 10^{-6}$; this threshold is based on Bonferroni correction for the total number of genes for which the study had SNP-level $p$-values in each of 12 GWA datasets (Table 2). We find that we are able to replicate up to 57.2% of gene hits in the WTCCC dataset using the PEGASUS method. We note that these four meta-analyses included the WTCCC dataset and are comprised of much larger sample sizes than our replication dataset.
| Source of GWA p-values                        | URL for Downloading p-values |
|----------------------------------------------|------------------------------|
| Psychiatric Genomics Consortium              | https://www.med.unc.edu/PGC/downloads |
| the International IBD Genetics Consortium   | http://www.ibdgenetics.org/downloads.html |
| GIANT consortium                             | http://www.broadinstitute.org/collaboration/giant/index.php/GIANT_consortium_data_files|
| Broad Institute                              | http://www.broadinstitute.org/ftp/pub/rheumatoid_arthritis/Stahl_etal_2010NG/ |
| DIAGRAM Consortium                           | http://diagram-consortium.org/downloads.html |
| Acute Lymphoblastic Leukemia (ALL) data      | Genotype data are available from dbGaP. (http://www.ncbi.nlm.nih.gov/gap), and steps to perform the GWA study are outlined in Xu et al (Xu et al. (2013)) |

**URLs for full SNP-level p-values from GWA datasets analyzed.**
TEXT S1

Connection between SKAT and PEGASUS tests

The underlying model for the SKAT test is a multiple linear (or logistic, depending on the phenotype of interest) mixed-model regression, given by Eq. 2; the associated variance component score statistic is given by Eq. 3. Under the null hypothesis of no association, the SKAT model reduces to the following:

\[ y_i = \alpha_0 + \alpha C_i + \epsilon_i \]  \hspace{1cm} (8)

In matrix notation, Eq. 8 can be written in matrix notation as \( Y = \alpha C + \epsilon \), where \( \epsilon \sim N(0, \sigma^2) \) and \( C \) is a matrix of covariates, and the estimates of the regression coefficients can be expressed as \( \hat{\alpha} = \alpha + (C^T C)^{-1} C^T \epsilon \). We define \( P = C(C^T C)^{-1} C^T \), which is a projection matrix as is \( I - P \). We substitute these values into the SKAT test statistic (Eq. 3), which gives the following:

\[ Q = [(I \ P)\epsilon]^T K [(I \ P)\epsilon] \]
\[ = \epsilon^T (I \ P) K (I \ P) \epsilon \] \hspace{1cm} (9)
\[ = \epsilon^T (I \ P) K \epsilon \]

Let \( d_1, \ldots, d_n \) be the eigenvalues of \( \sigma^2 [(I \ P) K] \). Then, the test statistic takes the form of \( \epsilon^T \text{diag}(d_1, \ldots, d_n) \epsilon \); this is a quadratic form that follows a mixture of \( \chi^2 \) distributions with weights given by \( d \).

In PEGASUS, the null distribution is a mixture of \( \chi^2 \) distributions with weights given by \( \lambda \), the eigenvalues of the LD matrix \( \Sigma \). If no covariates are considered and the variant weights are uniform for all variants (\( w_j = 1 \)), the SKAT null distribution becomes a mixture of \( \chi^2 \) distributions with mixture proportions given by the eigenvalues of the \( K = GWG^T \) matrix, which is a variance-covariance matrix similar to the PEGASUS LD matrix \( \Sigma \). Thus, under these circumstances, the two tests give similar results (Figure S15C-D).
Text S2

Additional significantly associated gene subnetworks for Attention-Deficit/Hyperactivity Disorder (ADHD), identified using PEGASUS gene scores as input to HotNet2

The subnetwork shown in Figure 5E contains \textit{FURIN}, a gene containing one SNP significantly associated with ADHD (GWA $p$-value $1.316 \times 10^{-5}$; \textit{Neale et al.} (2010)). \textit{FURIN} encodes the protease furin that processes latent precursor proteins into biologically active truncated BDNF molecules in the trans-Golgi network. Decreased levels of truncated BDNF have been shown to be associated with memory loss and learning impairment (\textit{Carlino et al.} (2013)). Another gene in the subnetwork, \textit{PACS1}, has been found to be moderately associated with years of education in a previous GWA study ($p$-value $4.9 \times 10^{-6}$; \textit{Rietveld et al.} (2013)). \textit{PACS1}, encoded by \textit{PACS1}, is a trans-golgi-membrane traffic regulator that binds furin; it has been shown to be involved in the localization of the protease furin to the trans-Golgi network (\textit{Wan et al.} (1998)). This gene has also been found to be mutated in cases of an unknown syndrome with intellectual disability (\textit{Schuurs-Hoel MAKERS et al.} (2012)). LRP1, or low density lipoprotein receptor-related protein 1, is encoded by the \textit{LRP1} gene and is a major receptor for apolipoprotein E (apoE), which transports lipids to the brain and also plays a role in neuronal repair (\textit{Fuentealba et al.} (2010)). LRP1 and apoE are also involved in mediating the clearance of amyloid $\beta$ 42 from the brain, and defective clearance of amyloid $\beta$ leads to accumulation in neurons, which contributes to Alzheimer’s Disease (\textit{Fuentealba et al.} (2010)). Collectively, we find that genes in this subnetwork play important roles in cell trafficking processes that may be involved in the pathology of neuropsychiatric and cognitive disorders such as Alzheimer’s Disease and intellectual disability.

A third subnetwork (Figure 5F) contains the genes \textit{RORB} and \textit{MPPED2}, both of which are moderately associated with years of education in previous GWA studies (GWA $p$-values $7.5 \times 10^{-4}$ and $6.7 \times 10^{-4}$, respectively; \textit{Rietveld et al.} (2013)). \textit{MPPED2} is also associated with information processing speed (\textit{Luciano et al.} (2011); GWA $p$-value $1.6 \times 10^{-5}$). \textit{MPPED2} is expressed in the fetal brain and is associated with WAGR syndrome whose symptoms include Wilms’ tumor, aniridia, genitourinary anomalies and retardation, but the gene’s function in the brain is still unclear (\textit{Chen et al.} (2010); \textit{Davis et al.} (2008)). The gene \textit{NR2F2}, which encodes the COUP-TFII transcription factor, is important in many aspects of neural development including neurogene-
sis, axogenesis, and differentiation (Naka et al. (2008)). RORB encodes the transcription factor RORB which is known to play a regulatory role in neurogenesis and has been found to be associated with bipolar disorder (McGrath et al. (2009)). The gene RARG encodes a retinoic acid receptor (retinoic acid receptor gamma) which makes a heterodimeric pair with a retinoid X receptor. The RXRG gene encodes one such retinoid X receptor (Maden (2007)). The retinoic acid receptor-retinoid X receptor heterodimeric pair are involved in mediating response to retinoic acid by binding to a DNA region containing a retinoic acid response element (RARE), which is bound to a corepressor protein and regulates transcription. Retinoic acid is very important in development of the nervous system, especially in patterning and neuronal differentiation (Maden (2007)). The genes in this subnetwork (Figure 5F) are thus likely involved in brain development. The genes in Figure 5D-F were found using VEGAS gene scores as input to HotNet2 as well.

Text S3

Additional significantly associated gene subnetworks for Waist-Hip Ratio (WHR), identified using PEGASUS gene scores as input to HotNet2

The second subnetwork found by HotNet2 (Leiserson et al. (2015)) using PEGASUS gene scores as input contains the gene VEGFA (vascular endothelial growth factor A), which is thought to mediate adipogenesis (Heid et al. (2010)). Serum levels of VEGFA are correlated with obesity (Heid et al. (2010)). VEGFA is also associated with angiogenesis (formation of new blood vessels) and for these reasons, VEGFA has been posited to underlie the association between childhood obesity and increased risk for atherosclerosis (Siervo et al. (2012)). The growth factor encoded by VEGFB (vascular endothelial growth factor B), which is also contained in the subnetwork, is involved in endothelial targeting of fatty acids to peripheral tissues. Mice deficient in VEGFB show decreased uptake of lipids by heart, muscle and brown adipose tissue, which are mitochondria rich and use fatty acids as an energy source, and increased accumulation of lipids in white adipose tissue instead, ultimately resulting in increased body weight (Hagberg et al. (2010)). FLT1, which encodes the vascular endothelial growth factor receptor 1, and NRP1 or neurophilin 1, encoded by the NRP1 gene, are a receptor and co-receptor, respectively for VEGFB. Mice lacking the FLT1 gene and mice deficient in NRP1 both show down-regulation of
fatty acid transport proteins in the heart, suggesting that VEGFB functions via FLT1 and NRP1 signaling (HAGBERG et al. (2010)). In this subnetwork, we see genes known to be associated with obesity and lipid trafficking; taken together, this result elucidates the mechanisms of action of VEGFA, which contains a known GWA study association for WHR (SNP $p$-value $1.38 \times 10^{-10}$; HEID et al. (2010)) and VEGFB, which is moderately associated with WHR (SNP $p$-value $7.2 \times 10^{-3}$; HEID et al. (2010)). These genes were found using VEGAS gene scores as input to HotNet2 as well.
Log-log plots of minSNP gene scores ($< 10^{-8}$ where possible) and corresponding PEGASUS gene scores for the 12 datasets analyzed in this study (Table 2). The points are colored by the z-score for the number of SNPs in the gene in each study, where red represents the highest possible z-score and yellow the lowest. We find that minSNP gene scores are almost always lower than PEGASUS gene scores.
Figure S2

Quantile-quantile plots comparing the base-10 logarithm of PEGASUS gene scores against the base-10 logarithm of minSNP gene scores for the 12 datasets analyzed in this study (Table 2). Each point represents a gene and is colored yellow, red or blue based on gene length (measured by the number of SNPs in the gene ± 50 kb boundary) percentile: 0-25%, 25-75%, and 75-100%, respectively. We find that minSNP gene scores are smaller than PEGASUS gene scores and decrease with increasing number of SNPs in a gene.
Log-log (base-10 logarithm) plots of PEGASUS against VEGAS gene scores for the 12 datasets analyzed in this study (Table 2). There is high concordance between gene score results from the two methods for all genes except those with gene scores $\leq 10^{-6}$ (below red dashed line); such genes can be ranked by gene score using PEGASUS, but not VEGAS.
1 - Local FDR (IFDR) versus minSNP gene scores with gene score threshold indicated at IFDR of 0.05 for the 12 datasets analyzed in this study (Table 2). The black squares represent the gene score threshold for minSNP gene scores used as input to HotNet2 analysis. The gene score threshold is determined by finding the gene score where IFDR reaches 0.05.
1 - Local FDR (IFDR) versus VEGAS gene scores with gene score threshold indicated at the first “elbow” point in the graph for the 12 datasets analyzed in this study (Table 2). The black squares represent the gene score threshold for VEGAS gene scores used as input to HotNet2 analysis. The gene score threshold is determined by finding the first “elbow” point in the graph.
Figure S6

1 - Local FDR (IFDR) versus PEGASUS gene scores with gene score threshold indicated at the first “elbow” point in the graph for the 12 datasets analyzed in this study (Table 2). The black squares represent the gene score threshold for PEGASUS gene scores used as input to HotNet2 analysis. The gene score threshold is determined by finding the first “elbow” point in the graph.
Figure S7

Quantile-quantile plots comparing the base-10 logarithm of PEGASUS gene scores against the base-10 logarithm of minSNP gene scores, multiplied by gene length. Each point represents a gene and is colored yellow, red or blue based on gene length (measured by the number of SNPs in the gene ± 50 kb boundary) percentile: 0-25%, 25-75%, and 75-100%, respectively. minSNP gene scores, when corrected for gene length by multiplying by the number of SNPs in a gene, are still lower for genes with higher gene length.
Figure S8

Quantile-quantile plots comparing the base-10 logarithm of PEGASUS gene scores against the base-10 logarithm of minSNP gene scores from the Beta(1, gene length) distribution for the 12 datasets analyzed in this study (Table 2). Each point represents a gene and is colored yellow, red or blue based on gene length (measured by the number of SNPs in the gene ± 50 kb boundary) percentile: 0-25%, 25-75%, and 75-100%, respectively. minSNP gene scores, when corrected for gene length by calculating a p-value for the gene score from the Beta(1, gene length) distribution, are still lower for genes with higher gene length.
Additional significantly associated gene subnetworks for ADHD identified using PEGASUS gene scores and HotNet2. Circles represent genes in each subnetwork and are colored by heat score (negative log-transformed PEGASUS gene scores); the color bar indicates the lowest heat score (blue or “cold” genes) and highest heat score (red or “hot” genes) in each subnetwork. Lines between genes indicate a gene interaction from the HINT database (Das and Yu (2012)).
**Figure S10**

HotNet2 results for Ulcerative Colitis (UC) using minSNP gene scores. We performed HotNet2 analysis using minSNP gene scores for Ulcerative Colitis and found these significant gene interaction subnetworks ($p \leq 0.05$). Subnetworks containing only genes with $p_g < 10^{-5}$ are not shown in this figure. Circles represent genes in each subnetwork and are colored by heat score (negative log-transformed minSNP gene scores); the color bar indicates the lowest heat score (blue or “cold” genes) and highest heat score (red or “hot” genes) in each subnetwork. Lines between genes indicate a gene interaction from the HINT database (Das and Yu (2012)). minSNP
subnetworks typically show “star-shaped” networks with many low scoring genes that are likely artifacts.

**Figure S11**

**HotNet2 results for Ulcerative Colitis (UC) using VEGAS gene scores.** We performed HotNet2 analysis using VEGAS gene scores for Ulcerative Colitis and found these significant gene interaction subnetworks ($p \leq 0.05$). Subnetworks containing only genes with $p_g < 10^{-5}$ are not shown in this figure. Circles represent genes in each subnetwork and are colored by heat score (negative
log-transformed VEGAS gene scores); the color bar indicates the lowest heat score (blue or “cold” genes) and highest heat score (red or “hot” genes) in each subnetwork. Lines between genes indicate a gene interaction from the HINT database (Das and Yu (2012)). These subnetworks are missing potentially biologically relevant results that can be found with PEGASUS due to its higher precision gene scores (Figure 4).

**Figure S12**

Additional significantly associated subnetworks for Ulcerative Colitis (UC) identified using PEGASUS gene scores and HotNet2. We performed HotNet2 analysis using PEGASUS gene scores for Ulcerative Colitis and found these significant gene interaction subnetworks ($p \leq 0.05$) in addition to the subnetworks in Figure 5A-C. Subnetworks containing only genes with $p_g \leq 10^{-5}$ are not shown in this figure. Circles represent genes in each subnetwork and are colored by heat.
score (negative log-transformed PEGASUS gene scores); the color bar indicates the lowest heat score (blue or “cold” genes) and highest heat score (red or “hot” genes) in each subnetwork. Lines between genes indicate a gene interaction from the HINT database (DAS and Yu (2012)).

**Figure S13**

**Simulation Part 1 - Choosing causal genes and SNPs:**

1. **KEGG Pathway Database**
   - Choose 4 pathways at random with >20 genes each
   - Randomly sample 20% of genes in each pathway
   - Run Tagger to find tag SNPs with \( r^2 < 0.2 \)
   - Use WTCCC controls (N = 2900) as reference for LD
   - 382 tag SNPs
   - Choose 1, 2, or 5 tag SNPs from each gene
   - 123 causal SNPs
   - Assign all causal SNPs in each gene effect size of 1.2 or 2

**Simulation Part 2 - GWA study on simulated phenotype:**

1. Simulated phenotypes for each WTCCC indiv. based on causal SNPs (see Methods)
2. Perform GWAS in PLINK using logistic regression
3. Top 4 PCs from PCA to control for ancestry
4. GWAS p-values
5. Genome-wide significant SNPs from real GWA data introduce spurious associations
6. GWAS p-values + spurious associations
7. Simulated gene scores

**Steps to simulate GWA data with known genomic architecture.** We performed a GWA study for simulated phenotype data with known underlying true causal genes based on the approach described in Wojcik et al (WOJCJ et al. (2015)). We first choose casual genes from the KEGG Pathway Database (KANEHISA (1997); KANEHISA et al. (2012)), find tag SNPs using WTCCC control individuals as reference for LD (WTCCC (2007)), choose 1,2, or 5 tag SNPs from each gene to be causal SNPs and then randomly assign all SNPs in a gene an odds ratio of 1.2 or 2. We assign case/control status to the WTCCC control individuals based on their minor allele dosage at each causal SNP (see Subjects and Methods), and we perform logistic regression on minor allele dosage and simulated phenotype, using the top four principal components as covariates in the logistic regression to control for ancestry, to obtain GWA SNP-level \( p \)-values. Simulated gene-level \( p \)-values are then generated from SNP-level using PEGASUS, VEGAS and minSNP.
Receiver Operating Characteristic (ROC) Curves from GWA simulations Conducted with Varying Parameters. We performed a GWA study for a simulated phenotype with known underlying true causal genes (see Subjects and Methods), and determined true positive rate (TPR; genes truly associated with phenotype that were identified as such) and false positive rate (FPR; genes identified as causal by a gene score method that were not truly associated with the simulated phenotype) for minSNP, VEGAS, SKAT and PEGASUS for various gene score thresholds (see Subjects and Methods). A-C show ROC curves for simulations with 20%, 40%, and 60% spurious GWA hits, respectively, from real GWA data for Crohn’s Disease (CD) added to GWA p-values for a simulated phenotype. D-F show ROC curves for simulations with 20%, 40%, and 60% spurious GWA hits, respectively, from real GWA data for Rheumatoid Arthritis (RA) added to GWA p-values for a simulated phenotype. H-J show ROC curves for simulations with 20%, 40%, and 60% spurious GWA hits, respectively, from real GWA data for Ulcerative Colitis (UC) added to GWA p-values for a simulated phenotype. We find that PEGASUS and VEGAS outperform minSNP and SKAT with higher TPRs at very low FPRs for every simulation.
Quantile-quantile plots comparing SKAT and PEGASUS $p$-values. We calculated gene-level $p$-values for the Acute Lymphoblastic Leukemia (ALL) (Xu et al. (2013)) and the WTCCC Type 2 Diabetes (T2D) (WTCCC (2007)) datasets using the SKAT method with suggested weights ($\overline{w_j} = \text{Beta}(\text{MAF}_j; 1, 25)$) and no weights ($w_j = 1$ for all variants) (Wu et al. (2010, 2011)) and PEGASUS; we note that SKAT requires genotype data as input, which is why these two phenotypes were analyzed here. We show the resulting $\log_{10}$ PEGASUS $p$-values versus $\log_{10}$ SKAT $p$-values for the two datasets. For both ALL and T2D, we find that SKAT $p$-values calculated with the suggested weights and PEGASUS $p$-values are correlated, with $r$ values of 0.4445 and 0.4933, respectively ($p < 2 \times 10^{-16}$ for both datasets). When the unweighted SKAT test is performed, we find that SKAT $p$-values and PEGASUS $p$-values are correlated, with $r$ values of 0.9609 and 0.9406, respectively ($p < 2 \times 10^{-16}$ for both datasets).
Mean minSNP and PEGASUS gene scores versus gene length for the 12 datasets analyzed in this study (Table 2). Each point represents the mean gene score ± standard error of the mean (SE) for a given number of SNPs in a gene. We find that the mean minSNP gene score (blue) decreases with increasing number of SNPs in a gene, however, PEGASUS gene scores (orange) do not show this trend.
### Table S1

| Disease or Trait | Level of Significance for gene score ($10^{-6}$) | # of significant genes (min-SNP) | % significant genes (min-SNP) | # of significant genes (PEGASUS) | % significant genes (PEGASUS) | # of significant genes (VEGAS) | % significant genes (VEGAS) |
|-----------------|---------------------------------------------|-------------------------------|-------------------------------|---------------------------------|-------------------------------|-------------------------------|-------------------------------|
| ADHD            | 2.81                                        | 1                             | 0.01                          | 0                               | 0                             | 0                             | 0                             |
| (Neale et al. (2010)) |                                        |                                |                               |                                 |                               |                               |                               |
| ALL             | 2.78                                        | 29                            | 0.16                          | 10                              | 0.06                          | 10                            | 0.06                          |
| (Xu et al. (2013)) |                                        |                                |                               |                                 |                               |                               |                               |
| BIP             | 2.81                                        | 47                            | 0.26                          | 17                              | 0.1                           | 17                            | 0.1                           |
| (Sklar et al. (2011)) |                                        |                                |                               |                                 |                               |                               |                               |
| BMI             | 2.83                                        | 96                            | 0.54                          | 56                              | 0.32                          | 56                            | 0.32                          |
| (Speliotes et al. (2010)) |                                        |                                |                               |                                 |                               |                               |                               |
| CD              | 2.88                                        | 431                           | 2.48                          | 256                             | 1.47                          | 249                           | 1.43                          |
| (Franke et al. (2010)) |                                        |                                |                               |                                 |                               |                               |                               |
| Height          | 2.83                                        | 834                           | 4.71                          | 404                             | 2.28                          | 397                           | 2.24                          |
| (Lango Allen et al. (2010)) |                                        |                                |                               |                                 |                               |                               |                               |
| MDD             | 2.81                                        | 16                            | 0.09                          | 0                               | 0                             | 0                             | 0                             |
| (Ripke et al. (2013)) |                                        |                                |                               |                                 |                               |                               |                               |
| RA              | 2.80                                        | 252                           | 1.41                          | 180                             | 1.01                          | 183                           | 1.03                          |
| (Stahl et al. (2010)) |                                        |                                |                               |                                 |                               |                               |                               |
| SCZ             | 2.81                                        | 250                           | 1.41                          | 55                              | 0.31                          | 55                            | 0.31                          |
| (Ripke et al. (2011)) |                                        |                                |                               |                                 |                               |                               |                               |
| T2D             | 2.82                                        | 54                            | 0.3                           | 11                              | 0.06                          | 10                            | 0.06                          |
| (Morris et al. (2012)) |                                        |                                |                               |                                 |                               |                               |                               |
| UC              | 2.80                                        | 980                           | 5.5                           | 190                             | 1.07                          | 191                           | 1.07                          |
| (Anderson et al. (2011)) |                                        |                                |                               |                                 |                               |                               |                               |
| WHR             | 2.83                                        | 50                            | 0.28                          | 17                              | 0.1                           | 18                            | 0.1                           |
| (Heid et al. (2010)) |                                        |                                |                               |                                 |                               |                               |                               |

**Number of significant genes and percentage of significant genes (out of the total number of genes considered) for minSNP, PEGASUS and VEGAS gene scores.** Significance is based on Bonferroni correction for the total number of genes for which the study had SNP-level $p$-values in each of 12 GWA datasets (Table 2). We find that minSNP always finds more associated genes than the other two methods. PEGASUS and VEGAS typically find similar numbers of associated genes.
Table S2

| Disease or Trait | Reference Data | # WTCCC Cases in Reference Data | # Non-WTCCC Cases in Reference Data | # of PEGASUS Hits in Reference Data replicated in WTCCC data | Total # of PEGASUS hits in Reference Data | % PEGASUS hits replicated in WTCCC data (Column 5/Column 6) |
|------------------|----------------|---------------------------------|-------------------------------------|---------------------------------------------------------------|----------------------------------------|---------------------------------------------------------------|
| BIP              | SKLAR et al. (2011) | 1,571                           | 5,910                               | 0                                                              | 17                                     | 0.0                                                           |
| CD               | FRANKE et al. (2010) | 1,747                           | 4,586                               | 11                                                             | 254                                    | 4.3                                                           |
| RA               | STAHL et al. (2010)  | 1,525                           | 4,014                               | 103                                                            | 180                                    | 57.2                                                          |
| T2D              | MORRIS et al. (2012) | 1,924                           | 10,247                              | 1                                                              | 11                                     | 9.1                                                           |

**Replication of PEGASUS gene hits in WTCCC datasets.** We conducted a replication experiment for PEGASUS gene hits for the 12 GWA datasets in this study in WTCCC data for Bipolar Disorder (BIP), Crohn’s Disease (CD), Rheumatoid Arthritis (RA) and Type 2 Diabetes (T2D). A “hit” is a gene with a gene score \( p_g < 2.8 \times 10^{-6} \); this threshold is based on Bonferroni correction for the total number of genes for which the study had SNP-level \( p \)-values in each of 12 GWA datasets (Table 2). We find that we are able to replicate up to 57.2% of gene hits in the WTCCC dataset using the PEGASUS method. We note that these four meta-analyses included the WTCCC dataset and are comprised of much larger sample sizes than our replication dataset.
Table S3

| Source of GWA p-values                                    | URL for Downloading p-values                                      |
|-----------------------------------------------------------|------------------------------------------------------------------|
| Psychiatric Genomics Consortium                           | https://www.med.unc.edu/pgc/downloads                             |
| the International IBD Genetics Consortium                | http://www.ibdgenetics.org/downloads.html                        |
| GIANT consortium                                         | http://www.broadinstitute.org/collaboration/giant/index.php/     |
|                                                           | GIANT_consortium_data_files                                      |
| Broad Institute                                           | http://www.broadinstitute.org/ftp/pub/rheumatoid_arthritis/      |
|                                                           | Stahl_etal_2010NG/                                              |
| DIAGRAM Consortium                                       | http://diagram-consortium.org/downloads.html                     |
| Acute Lymphoblastic Leukemia (ALL) data                   | Genotype data are available from dbGaP. (http://www.ncbi.nlm.nih.gov/gap), and steps to perform the GWA study are outlined in Xu et al (Xu et al. (2013)) |

URLs for full SNP-level p-values from GWA datasets analyzed.
Algorithm 1 permSNP

1: Calculate the observed gene-level test statistic for gene with $n$ SNPs

$$Q_{obs} = \frac{\sum_{i=1}^{n} q_i}{n}$$  \hspace{1cm} (10)

2: For $M$ case-control permutations, calculate the permuted gene-level test statistic and record whether the permuted statistic is greater than the observed statistic

3: for $j = 1$ to $M$ do

4: $$Q_j^* = \frac{\sum_{i=1}^{n} q_i^*}{n}$$  \hspace{1cm} (11)

$$I_j = \begin{cases} 1 & \text{if } Q_j^* > Q_{obs} \\ 0 & \text{otherwise} \end{cases}$$  \hspace{1cm} (12)

5: end for

6: Calculate gene-level $p$-value

$$p_g = \frac{\sum_{j=1}^{M} I_j}{M}$$  \hspace{1cm} (13)
Text S1

Connection between SKAT and PEGASUS tests

The underlying model for the SKAT test is a multiple linear (or logistic, depending on the phenotype of interest) mixed-model regression, given by Eq. 2; the associated variance component score statistic is given by Eq. 3. Under the null hypothesis of no association, the SKAT model reduces to the following:

$$y_i = \alpha_0 + \alpha'C_i + \epsilon_i$$  (8)

In matrix notation, Eq. 8 can be written in matrix notation as $Y = \alpha'C + \epsilon$, where $\epsilon \sim \mathcal{N}(0, \sigma^2)$ and $C$ is a matrix of covariates, and the estimates of the regression coefficients can be expressed as $\hat{\alpha} = \alpha + (C^TC)^{-1}C^T\epsilon$. We define $P = C(C^TC)^{-1}C^T$, which is a projection matrix as is $I - P$. We substitute these values into the SKAT test statistic (Eq. 3), which gives the following:

$$Q = [(I - P)\epsilon]^TK[(I - P)\epsilon]$$
$$= \epsilon^T(I - P)K(I - P)\epsilon$$  (9)
$$= \epsilon^T(I - P)K\epsilon$$

Let $d = d_1, \ldots, d_n$ be the eigenvalues of $\sigma^2[(I - P)K]$. Then, the test statistic takes the form of $\epsilon^T diag(d_1, \ldots, d_n)\epsilon$; this is a quadratic form that follows a mixture of $\chi^2$ distributions with weights given by $d$.

In PEGASUS, the null distribution is a mixture of $\chi^2$ distributions with weights given by $\lambda$, the eigenvalues of the LD matrix $\Sigma$. If no covariates are considered and the variant weights are uniform for all variants ($w_j = 1$), the SKAT null distribution becomes a mixture of $\chi^2$ distributions with mixture proportions given by the eigenvalues of the $K = GWG'$ matrix, which is a variance-covariance matrix similar to the PEGASUS LD matrix $\Sigma$. Thus, under these circumstances, the two tests give similar results (Figure S15C-D).
Text S2

Additional significantly associated gene subnetworks for Attention-Deficit/Hyperactivity Disorder (ADHD), identified using PEGASUS gene scores as input to HotNet2

The subnetwork shown in Figure 5E contains FURIN, a gene containing one SNP significantly associated with ADHD (GWA $p$-value $1.316 \times 10^{-5}$; NEALE et al. (2010)). FURIN encodes the protease furin that processes latent precursor proteins into biologically active truncated BDNF molecules in the trans-Golgi network. Decreased levels of truncated BDNF have been shown to be associated with memory loss and learning impairment (CARLINO et al. (2013)). Another gene in the subnetwork, PACS1, has been found to be moderately associated with years of education in a previous GWA study ($p$-value $4.9 \times 10^{-6}$; RIETVELD et al. (2013)). PACS1, encoded by PACS1, is a trans-golgi-membrane traffic regulator that binds furin; it has been shown to be involved in the localization of the protease furin to the trans-Golgi network (WAN et al. (1998)). This gene has also been found to be mutated in cases of an unknown syndrome with intellectual disability (SCHUURS-HOEIJMAKERS et al. (2012)). LRP1, or low density lipoprotein receptor-related protein 1, is encoded by the LRP1 gene and is a major receptor for apolipoprotein E (apoE), which transports lipids to the brain and also plays a role in neuronal repair (FUENTEALBA et al. (2010)). LRP1 and apoE are also involved in mediating the clearance of amyloid $\beta$ 42 from the brain, and defective clearance of amyloid $\beta$ leads to accumulation in neurons, which contributes to Alzheimer’s Disease (FUENTEALBA et al. (2010)). Collectively, we find that genes in this subnetwork play important roles in cell trafficking processes that may be involved in the pathology of neuropsychiatric and cognitive disorders such as Alzheimer’s Disease and intellectual disability.

A third subnetwork (Figure 5F) contains the genes RORB and MPPED2, both of which are moderately associated with years of education in previous GWA studies (GWA $p$-values $7.5 \times 10^{-4}$ and $6.7 \times 10^{-4}$, respectively; RIETVELD et al. (2013)). MPPED2 is also associated with information processing speed (LUCIANO et al. (2011): GWA $p$-value $1.6 \times 10^{-5}$). MPPED2 is expressed in the fetal brain and is associated with WAGR syndrome whose symptoms include Wilms’ tumor, aniridia, genitourinary anomalies and retardation, but the gene’s function in the brain is still unclear (CHEN et al. (2010); DAVIS et al. (2008)). The gene NR2F2, which encodes the COUP-TFI transcription factor, is important in many aspects of neural development including neurogene-
sis, axogenesis, and differentiation (Naka et al. (2008)). *RORB* encodes the transcription factor RORB which is known to play a regulatory role in neurogenesis and has been found to be associated with bipolar disorder (McGrath et al. (2009)). The gene *RARG* encodes a retinoic acid receptor (retinoic acid receptor gamma) which makes a heterodimeric pair with a retinoid X receptor. The RXRG gene encodes one such retinoid X receptor (Maden (2007)). The retinoic acid receptor-retinoid X receptor heterodimeric pair are involved in mediating response to retinoic acid by binding to a DNA region containing a retinoic acid response element (RARE), which is bound to a corepressor protein and regulates transcription. Retinoic acid is very important in development of the nervous system, especially in patterning and neuronal differentiation (Maden (2007)). The genes in this subnetwork (Figure 5F) are thus likely involved in brain development. The genes in Figure 5D-F were found using VEGAS gene scores as input to HotNet2 as well.
Additional significantly associated gene subnetworks for Waist-Hip Ratio (WHR), identified using PEGASUS gene scores as input to HotNet2

The second subnetwork found by HotNet2 (Leiserson et al. (2015)) using PEGASUS gene scores as input contains the gene VEGFA (vascular endothelial growth factor A), which is thought to mediate adipogenesis (Heid et al. (2010)). Serum levels of VEGFA are correlated with obesity (Heid et al. (2010)). VEGFA is also associated with angiogenesis (formation of new blood vessels) and for these reasons, VEGFA has been posited to underlie the association between childhood obesity and increased risk for atherosclerosis (Siervo et al. (2012)). The growth factor encoded by VEGFB (vascular endothelial growth factor B), which is also contained in the subnetwork, is involved in endothelial targeting of fatty acids to peripheral tissues. Mice deficient in VEGFB show decreased uptake of lipids by heart, muscle and brown adipose tissue, which are mitochondria rich and use fatty acids as an energy source, and increased accumulation of lipids in white adipose tissue instead, ultimately resulting in increased body weight (Hagberg et al. (2010)). FLT1, which encodes the vascular endothelial growth factor receptor 1, and NRP1 or neuropilin 1, encoded by the NRP1 gene, are a receptor and co-receptor, respectively for VEGFB. Mice lacking the FLT1 gene and mice deficient in NRP1 both show down-regulation of fatty acid transport proteins in the heart, suggesting that VEGFB functions via FLT1 and NRP1 signaling (Hagberg et al. (2010)). In this subnetwork, we see genes known to be associated with obesity and lipid trafficking; taken together, this result elucidates the mechanisms of action of VEGFA, which contains a known GWA study association for WHR (SNP p-value $1.38 \times 10^{-10}$; Heid et al. (2010)) and VEGFB, which is moderately associated with WHR (SNP p-value $7.2 \times 10^{-3}$; Heid et al. (2010)). These genes were found using VEGAS gene scores as input to HotNet2 as well.
