1. Introduction

Cold extrusion processes provide high surface quality and precise sizes of stamped blanks and components. This, in turn, reduces or eliminates the need for additional machining by cutting [1, 2]. The most common conventional extrusion techniques are the longitudinal (inverse and direct) extrusion methods, which are characterized by the flow of the...
extruded metal along the longitudinal axis of symmetry [3]. The components that are complex in shape should be made by using the techniques of transverse (radial and lateral) and combined transverse-longitudinal extrusion [2]. In this case, stamps with matrices are used, whose transverse (circular or channel) receiving cavity is made detachable, mainly on a horizontal (transverse) plane [4].

Combining the longitudinal and transverse extrusion schemes is necessary to create more complex deformation techniques. This makes it possible to fabricate, in a single run, solid and hollow components with flanges or rames, with deep cavities, or other configurations. Depending on the nature of the combination of simple transverse and longitudinal extrusion schemes in a single combined process, the techniques are divided into combined and consistent, over time or along the path of deformation, extrusion techniques. The combined techniques are characterized by the presence of one common site or adjacent deformation sites and several possible directions for a blank’s metal outflow. The use of a combination of simple deformation schemes is mainly aimed at optimizing the strength regime to improve the resilience of the tool and the stability of a cold deformation process [1, 4]. A series of combined extrusion techniques aim to enhance the capabilities of punching technologies by complicating the shape of the components and providing the required specifications of parts [5].

2. Literature review and problem statement

Our analysis of publications is preceded by a generalization of the techniques for consistent radial-longitudinal extrusion, designed to obtain hollow components. There are two main types of these techniques: the extrusion schemes with the expansion of metal (Table 1, row A) [5–9] and the extrusion schemes with the compression of metal at its radial flow (Table 1, row B) [5, 10–12].

Group A extrusion schemes are distinguished by the consistent execution of radial and longitudinal extrusion operations. In this case, the radial extrusion of the metal occurs with the expansion, that is, by the flow of the metal from the center of a blank to the periphery. When the «matrix-free extrusion» techniques are employed, the metal is extruded simultaneously through the lateral and lower end of the blank (A1) or through the side surface of the blank (A2) [5, 6]. These techniques are applied to make deep hollow vessels, which significantly reduces the force of deformation compared to the use of reverse extrusion [4, 7]. The extrusion techniques to fabricate components from a solid blank as a result of the developed radial current, which is replaced by a straight (A3 scheme) or reverse current of the deformed metal (A4 scheme), are used, respectively, for the manufacture of deep casings [5, 7] and cups [8, 9]. The process of deformation in line with the scheme of radial-direct extrusion with expansion makes it possible to reduce the forces of deformation by reducing the area of contact between an active deforming tool and a blank. However, this is accompanied by a marked increase in the specific loads on the tool, which limits the possibilities of the process.

The radial-direct extrusion techniques from group B differ in that they imply the radial extrusion of metal in the direction from the periphery to the center. That is why they are termed the techniques of consistent radial-direct extrusion with compression [5, 10–12]. Depending on the tool used, the way the metal is fed at the direct current stage and, accordingly, the outflow degree of freedom, several extrusion schemes are distinguished (B1 and B2 schemes). The B3 scheme is characterized by the use of a conical mandrel capable of recurrent movement, which is necessary to obtain components with variable wall thickness [10]. When profiling a mandrel (B4 scheme), it is possible to make components with the ribbed inner surface. Subject to providing the mandrel with an independent drive for longitudinal movement and turning around the axis, one could get components with a profiled inner surface [10, 11] or with many spiral grooves on the inner wall [12].

In recent years, many researchers have shown interest in the processes of combined radial-longitudinal extrusion. Analysis of force and deformation regimes of these processes is performed mainly experimentally, by applying methods of finite elements (FEM) and upper estimate. Work [7] investigated the impact of some important structural geometric parameters of the process of sequential radial-direct extrusion (the flange thickness, the size of the ring gap, the mandrel radius) on the emergence and fluctuations of the load. However, the conclusion that the counterpunch radius and the curvature radii of the tool’s transition sections have little impact on the formation of the load on the punch and the counter punch is questionable. Paper [13] describes the strength characteristics of the process of...
A model of the process using the simplest velocity fields of parallel current was proposed in [20] for the axisymmetric process of the radial-direct extrusion of components, the type of casings. Similarly, by using the energy method, the process of the combined extrusion of a hollow part from an aluminum alloy was examined in [21] in order to establish the characteristics of energy consumption. The energy method helped establish a share of significant costs to overcome the forces of contact friction in the total energy of shape formation of hollow components in the process of cold extrusion. However, these solutions that employ the parallel current KPVF, that is, the kinematic modules (zones) of rectangular shape, which could not describe the deformation site of complex configuration, are also approximate in character.

Hollow components of the type of a sleeve are widespread in the industry and it is a relevant task to derive the estimation dependences in order to design the processes of their extrusion. This is due to the fact that, along with the above benefits of the combined processes, there are a series of challenges associated with the complex stressed-strained state of a blank under conditions of extreme loads and the nature of metal outflow [5, 10]. In this case, the focus should be on the development of refined mathematical models for the calculation of technological modes, and first of all, the force parameters at the combined flow of metal with compression, which is characterized by the increased hydrostatic pressure in a plastic zone. At the same time, the complexity of the tool geometry emphasizes the task of calculating the reduced pressure of the new kinematic modules of trapezoidal and triangular shapes with different types of borders.

Our analysis of literary data reveals that the main issue holding back the application of combined extrusion processes in the industry is the lack of recommendations for calculating and developing the technology and designing the tool.

3. The aim and objectives of the study

The aim of this study is to identify patterns of the course, as well as construct mathematical models for the calculation, of the energy-force modes of combined radial-direct extrusion with the compression of components such as sleeves on the conical mandrel.

To accomplish the aim, the following tasks have been set:
- to devise an estimation scheme of the combined radial-direct extrusion process with compression using modules with a non-parallel flow;
- to investigate the effect of the tool geometry on the force mode of the combined radial-direct extrusion process with compression;
- to conduct a comparative analysis of the force parameters of the extrusion process, obtained theoretically on the basis of the constructed mathematical model, with experimentally acquired data.

4. Theoretical analysis of the process of combined radial-direct extrusion with compression

4.1. Development of an estimation scheme for the combined radial-direct extrusion process with compression

The effective theoretical methods of calculating cold combined extrusion processes include the energy method [22–24]. To calculate the axisymmetric processes, the deformed volume...
of a blank is split into axisymmetric kinematic modules with the corresponding kinematically possible velocity fields (KPVF). In this case, the complexity of the shape of the profiled blanks requires the development of new kinematic modules of trapezoidal and triangular shape. The calculation of the power of plastic deformation forces inside a kinematic module, the cutting forces with the adjoining modules, and the friction forces at the surface of the tool was considered in works [25–27]. It has been established that it is difficult to obtain an analytical expression of the power of the forces of deformation and impossible to use the linearization of deformation rates. It has been proposed to apply the upper estimate of the deformation rates power by Cauchy-Bunyakovsky or cubature formulæ [26, 27]. Such calculations are required by the triangular modules with a sloping curved or straight-line boundary or the curvilinear modules of different configurations.

Consider the estimation scheme of the process of combined radial-direct extrusion with compression, including triangular kinematic modules 2 and 3 with curvilinear and straight-line borders, respectively, and rigid modules 1 and 4.

![Fig. 1. Estimation scheme of the process of combined radial-direct extrusion with compression](image)

The KPVF of rigid modules 1 and 4 takes the form:

$$
\begin{align*}
V_{i_1} & = -\frac{C}{\mu} V_0, \\
V_{i_2} & = 0,
\end{align*}
$$

(1)

$$
\begin{align*}
V_{i_3} & = -\frac{2 C}{\mu} V_0, \\
V_{i_4} & = 0,
\end{align*}
$$

(2)

where

$$
C = \frac{R_i^2 - R_i^1}{2h(R_i + R)}.
$$

For modules of plastic deformation 2 and 3, the KPVF, the equations of curvilinear and sloping boundaries, the expression of the intensity of deformation rates $\dot{\epsilon}_i$ are given in Table 2.

The calculations of the power of the forces of deformation, the cutting and friction forces for kinematic modules 1, 2, and 4, are known and do not cause difficulties when fitting to the new estimation schemes.

### Equations of curvilinear boundaries and KPVF of plastic deformation modules

| No. | KPVF | Curvilinear boundary equations, expression of deformation rate intensity $\dot{\epsilon}_i$ |
|-----|------|------------------------------------------------------------------------------------------|
| 2   | $V_{i_1} = -\alpha V_0$; $V_{i_2} = \frac{R_i^2 - R_i^1}{2h} V_0$ | $Z_{wa} = \left(1 - \alpha \right) \left( \frac{r^2 - R_i^1}{R_i^2 - R_i^1} \right) + 1 \dot{h}$; $Z_{wc} = \alpha \left( \frac{r^2 - R_i^1}{R_i^2 - R_i^1} \right) \dot{h}$; $\dot{\epsilon}_i = \frac{R_i^2 - R_i^1}{\sqrt{3h^2}} V_0$ |
| 3   | $V_{i_1} = -2C \tan \beta \left( \frac{1}{2} \right) V_0$; $V_{i_2} = 1$ | $Z_{wa} = \frac{1}{\mu} \left( r - R \right)$, $Z_{wc} = \frac{1}{\mu} \left( r - R \right)$, $\dot{\epsilon}_i = \frac{C}{\sqrt{3h^2}} V_0 \left( \frac{r^2 + R_i^2 + R^2}{2} \right) + 2$ |

(3)

(4)

(5)

The power of deformation, cutting, and friction forces for kinematic module 3 was obtained in the analytical form:

$$
N_{C_{2,3}} = \frac{2\pi \sigma}{\sqrt{3}} V_0 \left( \frac{R_i^2 - R_i^1}{3R_i + R} \right) \left( \frac{R_i^2 - R^2}{4R_i (R_i^2 - R^2)} \right) - \alpha,
$$

(3)

$$
N_{C_{2,4}} = \frac{2\pi \mu}{\sqrt{3}} V_0 \left( \frac{R_i^2 - R^2}{2} + R(R_i - R) \right) \left( \frac{R_i^2 - R^2}{2(R_i + R)h} \right).
$$

(4)

$$
N_i = \frac{4\pi \sigma}{\sqrt{3}} V_0 \left( 1 + \frac{1}{\mu} \frac{1}{\tan \beta} \right) \left( \frac{R_i^2 - R^2}{2} + R(R_i - R) \right) \left( \frac{R_i^2 - R^2}{2(R_i + R)h} \right).
$$

(5)

However, the power of the deformation forces in module 3 is not expressed by elementary functions and requires the use of approximate upper estimates. We find the auxiliary values for the upper estimate of this magnitude:

$$
M = \frac{1}{V_0} \left( \frac{4\pi C_2}{3\sqrt{3}} \left( \frac{4\pi \sigma}{\sqrt{3}} V_0 \left( \frac{R_i^2 - R_i^1}{3R_i + R} \right) \left( \frac{R_i^2 - R^2}{4R_i (R_i^2 - R^2)} \right) - \alpha \right) \right).
$$

(6)

$$
M = \frac{2\pi \sigma}{\sqrt{3}} V_0 \left( \frac{R_i^2 - R_i^1}{3R_i + R} \right) \left( \frac{R_i^2 - R^2}{4R_i (R_i^2 - R^2)} \right) - \alpha.
$$

(7)

Thus, we derive an upper estimate of the power of the deformation forces in module 3 by Cauchy-Bunyakovsky:

$$
N_i \dot{\epsilon}_i < \sigma V_0 \sqrt{3M},
$$

(7)
where

\[ V = \frac{\pi}{3\sqrt{3}} (2R_1^2 + R_2^2 - 3R_1^2R_2) \]

– the scope of the module 3 integration region.

Using the upper estimate in the form (7) makes it possible to derive an analytical expression of the reduced deformation pressure in the following form:

\[
\overline{p} = \frac{1}{(R_2 - R_1)} \times \\
\left[ \frac{2}{\sqrt{3}} \left( R_1^2 \ln \frac{R_2}{R_1} + \frac{R_2^2 - R_1^2}{2} \right) + \frac{2}{\sqrt{3}} \left( \frac{R_1^2 - R_2^2}{2} \right) - \frac{2(\alpha R_2 - \alpha R_1)}{\sqrt{3}} \right] + \\
\left[ \frac{1}{\sqrt{3}} \left( 4\alpha^2 - 2\alpha + 1 \right) \right] \left( \frac{R_1^2 - R_2^2}{2} + R(R_2 - R_1) \right) \times \\
\left[ \frac{R_2^2 - R_1^2}{h} + \frac{2}{\sqrt{3}} \left( \frac{R_2^2 - R_1^2}{2} + R(R_2 - R_1) \right) \right] \\
\times \left[ \frac{4\alpha R_2 - R_1^2}{(R_1 + h)h} + \left( 1 + \frac{1}{\sqrt{3}h^2} \right) \right] + \\
\left[ \frac{4\alpha R_2 - R_1^2}{\sqrt{3}} \right] \left( \frac{R_2^2 - R_1^2}{R_2^2 - R_1^2} \right) \times \\
\left[ \frac{R_2^2 - R_1^2}{R_1 + h} \right] + \frac{2}{\sqrt{3}} R_1 (H_0 - \Delta H_0 - h) + \frac{\gamma Nm}{\pi} \right]
\]

where \( H_0 \) is the initial height of a blank; \( \Delta H_0 \) is the run.

This function could be considered as a function of the variable parameter \( \alpha \in (0,1) \), responsible for the shape of the kinematic module 2 borders, as well as the technological parameters \( R, R_1, R_2, h \) of the estimation scheme.

4.2. Analysis of the magnitude of the reduced pressure of the combined radial-direct extrusion process with compression

By proceeding to the dimensionless magnitudes relative to \( R_0 \) we analyze the behavior of the reduced pressure depending on the \( \alpha \in (0,h) \) parameter. We use a comparative analysis of the magnitude of the reduced pressure, obtained in the course of numerical integration in the form \( \overline{p} \), and using the upper estimate in the form \( \overline{p} \) given by (8). In this case, the process parameters correspond to the stage of deformation with the complete filling of the metal reversal zone in triangular module 3 (Fig. 2). The character of curves \( \overline{p} \) (solid line) and upper estimate \( \overline{p} \) (dotted line) is identical for different values \( \overline{h} = h / R_0 \), while the deviation of the upper estimate in the form (8) from \( \overline{p} \) does not exceed 0.2–1\%. In addition, for these curves, there is no displacement of the minimum point responsible for the optimal value of the parameter \( \alpha \). Thus, the use of the reduced pressure magnitude in the form \( \overline{p} \) according to (8) is justified and greatly facilitates the subsequent analysis of this magnitude. In further analysis, we use the upper estimate \( \overline{p} \) as the magnitude of the reduced pressure.

The variable parameter that optimizes the magnitude of the reduced pressure is the \( \alpha \in (0,1) \), parameter, responsible for the point \( B(R_0, dR) \) position and the shape of the kinematic module 2 boundaries (Fig. 3). The character of the curves at different values \( R = R_0 / R_1 \) is strikingly different in determining the minimum point of the reduced pressure magnitude, which corresponds to the optimal value of the parameter \( \alpha \). This is due to the component of the power of the cutting forces of kinematic modules 2 and 3, changing its sign depending on the ratios of geometric parameters and \( \alpha \). For \( R = 0.3 \), the minimum point corresponds to the equality to zero of the power of the cutting forces of kinematic modules 2 and 3; for the rest of the values, this condition is not met. The character of the curves at different values \( R = R_0 / R_1 \) also significantly depends on the component of the power of the cutting forces of kinematic modules 2 and 3; at \( R = 0.8 \), the minimum point corresponds to the condition \( Nc_{2,3} = 0 \) (Fig. 4). For the rest of the values \( R \), this condition is not met. In this case, an increase in \( R \) leads to a decrease in the magnitude of the reduced pressure and a shift towards reducing the optimal value of the parameter \( \alpha \).

![Fig. 2. Dependence of the reduced pressure on parameter \( \alpha \) at \( R = 0.3, R_1 = 0.5, h_0 = 1, \mu = 0.08 \) and different values \( \overline{h} \)](image)

![Fig. 3. Dependence of the reduced pressure on parameter \( \alpha \) at \( R = 0.8, h_0 = 0.5, h_0 = 1, \mu = 0.08 \) and different values \( \overline{R} \)](image)

![Fig. 4. Dependence of the reduced pressure on parameter \( \alpha \) at \( R = 0.3, h_0 = 0.3, h_0 = 1, \mu = 0.08 \) and different values \( \overline{R} \)](image)

We shall analytically determine the optimal value of the parameter \( \alpha \), corresponding to the optimal value of the
reduced pressure magnitude, employing the necessary condition of the minimum \( \overline{\sigma}_0 = 0 \). However, \( \overline{p} \) contains an expression of the absolute magnitude that depends on the parameter \( \alpha \), which makes it difficult to find a minimum point and corresponds to the different analytical expressions of the magnitude of reduced pressure, depending on the values in expression (3).

However, for some ratios of the deformation process geometric parameters, an analytical expression could be obtained for the optimal value of the parameter \( \alpha \):

\[
\alpha_{opt} = \frac{4R_1^2 + 3R_1R_2^2 - 7R_2^3}{8(R_2^3 - R_1^3)}
\]

at

\[
(R_2^3 - R_1^3)(3R_1 + R) - 4R(R_2^3 - R_1^3) > 0.
\]

This optimal value corresponds to the curve at \( R = 0.6 \) (Fig. 3) and the curves \( R = 0.5 \) and \( R = 0.6 \) (Fig. 4).

After substituting the optimal value of the parameter \( \alpha \) in the formula of the reduced pressure (8), further optimization for geometric parameters is possible, for example, for the angle of inclination of the forming mandrel \( \beta \) (Fig. 5). In order to obtain the components of the required thickness of the extruded wall, the magnitude \( \overline{p} \) must be fixed. In this case, the reduction of deformation efforts could be achieved by varying the inclination angle of the forming mandrel \( \beta \). Reducing the thickness of the extruded wall (an increase in \( \overline{R} \)) leads to an increase in the magnitude of the reduced pressure and a decrease in the optimal value of the angle of inclination of the forming mandrel. Moreover, for all ratios of geometric parameters, the nature of the curves is identical, the deviation of \( \beta \) from the optimal value towards a decrease leads to a more significant increase in the magnitude of the reduced pressure.

\begin{figure}[h]
\centering
\includegraphics[width=0.5\textwidth]{fig5.png}
\caption{Dependence of the reduced pressure for \( R = 0.6, R = 1.5, R_x = 0.3, \mu = 0.1 \) at different values of the parameter \( \beta \)}
\end{figure}

It has been established that among the relative geometric parameters, the magnitude \( \overline{p} \) is largely affected by the relative thickness of the extruded wall \( \overline{S} = \overline{R} - \overline{R} \) and the inclination angle of the forming mandrel \( \beta \). With the increase in the magnitude \( \overline{R} \), that is with a decrease in the thickness of the extruded wall, the magnitude of reduced pressure increases, which is associated with an increase in the degree of deformation. In this case, the optimal value of the inclination angle of the forming mandrel \( \beta \) decreases; the range of variation of this parameter is within 20° to 30° for different ratios of the deformation process.

\section{5. Comparative analysis of theoretical and experimental data on the force mode of the combined radial-direct extrusion process with compression}

In order to verify the adequacy of the acquired estimation data, experimental studies were conducted on the extrusion of hollow components by the combined radial-direct extrusion with compression (Fig. 6, a). Components from lead alloy and AA1135 were extruded. A distortion in the dividing grid in zone 2 of the turn in the direct and radial extrusion confirms the validity of the choice of the configuration of kinematic module 2 (Fig. 6, b). The study of the stressed-strained state based on FEM and experimental data on the force mode of the radial-direct extrusion process with compression is given in detail in work [9].

\begin{figure}[h]
\centering
\includegraphics[width=0.5\textwidth]{fig6.png}
\caption{Components obtained by combined radial-direct extrusion with compression: \( a \) – extruded samples from the AA1135; \( b \) – distortion of the dividing grid}
\end{figure}

Based on the results of our study, a chart was built demonstrating the dependence of the extrusion pressure on the course of the press slider at \( R_0 = 22.5 \text{ mm}, R_1 = 14 \text{ mm}, h = 11.5 \text{ mm}, H_0 = 30 \text{ mm} \) for the lead alloy blank (Fig. 7). Analysis of the experimentally acquired data (Fig. 7, point data) makes it possible to highlight three stages of the process during extrusion. In the first stage (I), there is a radial flow of the metal until it contacts the mandrel, and then the reversal of the metal and the onset of a direct flow. The flow of the metal is non-stationary and there is an increase in extrusion pressure. In the second stage (II), the flow of the metal is steady, and the extrusion pressure decreases slightly (the decrease is 5–10 %). The decrease in extrusion pressure is explained by a decrease in the area of the friction surface between the workpiece and the tool. In the final stage of the process (III), the deforming punch comes to the deformation site, giving rise to an increase in the pressure of extrusion. At the pressure-motion curve (Fig. 7, point data) this stage appears as an increase in extrusion pressure.

For these deformation process parameters, we derived, based on (9), the optimal value of the variable parameter \( \alpha_{opt} \). Next, based on the analytical expression of the reduced deformation pressure in the form (8) and for \( \overline{R} = 22.25 \text{ MPa} \), we derived the dependence of extrusion pressure on the course of the press slider. The deviation in data acquired from the proposed process calculation scheme (Fig. 7, solid line) from the experimentally obtained data does not exceed 13–15 %. In this case, the theoretical calculation corresponds to the slider’s run of up to 18 mm up to the degeneration of module 1.
Thus, the developed calculation scheme of the process of combined sequential radial-direct extrusion with compression could be used up to the degeneration of module 1, which corresponds to the slider run equal to $H_0 - h$.

6. Discussion of results of studying the force mode of the combined radial-direct extrusion process with compression

The use of triangular kinematic modules with curvilinear and straight-line boundaries has made it possible to describe the sites of intense deformation for the steady stage of the deformation process. Applying the upper estimate of the power of the deformation forces of kinematic module 3 of the triangular shape has made it possible to derive the magnitude of the reduced deformation pressure in the analytical form (7). Thus, we have solved the problem of calculating the reduced pressure of the new kinematic modules of triangular shapes of type 2 and 3 with different types of boundaries with the complexity of the shape of the deformation sites and the tool geometry. The resulting optimal value of parameter $a$ (9) has made it possible to analyze a change in the magnitude of the reduced deformation pressure (8) at different ratios of the process geometric parameters. It has been established that the optimal inclination angle values of the forming mandrel $\beta$ lie between $20^\circ$ and $30^\circ$ for different ratios of the deformation process (Fig. 5). In this case, the developed calculation scheme of the combined radial-direct extrusion process with compression could also be used for a fixed configuration of the mandrel at the slider’s run of up to $H_0 - h$, which is a constraint on the use of the proposed estimation scheme.

To test the validity of the constructed mathematical model of the process, experimental studies were conducted on the extrusion of hollow components from lead alloy and AA1135 by the radial-direct extrusion with compression. The distortion of the dividing grid in zone 2 of the reversal of the direct and radial extrusion confirms the validity of the choice of the configuration of kinematic module 2 (Fig. 6, b). In the comparative analysis of the theoretically and experimentally acquired data on the force regime, the effectiveness of the developed calculation scheme of the process (Fig. 7) has been confirmed. In this case, the deviation of data obtained based on the proposed calculation scheme of the process from those experimentally acquired does not exceed 13–15 %.

Note that the power of deformation forces in the form (7) and the power of friction forces in the form (5) for kinematic module 3 could be used in various calculation schemes when changing the neighboring kinematic modules. Adjustments would be required only for the calculation of the power of the cutting forces.

It is promising to further develop the new curvilinear kinematic modules of different configurations, to advance the simplification techniques to calculate them and to study their integration into more complex estimation schemes of the combined extrusion processes.

7. Conclusions

1. The estimation scheme of the process of combined radial-direct extrusion with compression using triangular modules with curvilinear and rectilinear boundaries has been built. This has made it possible to derive an analytical expression of the reduced pressure at the slider’s run of up to $H_0 - h$.

2. The effect of the tool geometry on the force mode of the combined radial-direct extrusion process with compression has been investigated. It has been established that the magnitude of the reduced pressure is most influenced by the relative thickness of the extruded wall $\frac{H}{R} = \frac{H}{R}$ and the angle of inclination of the forming mandrel $\beta$. With decreasing thickness of the extruded wall, the magnitude of the reduced pressure increases, which is associated with an increase in the degree of deformation. In this case, the optimal value of the angle of inclination of the forming mandrel $\beta$ decreases and is in the range from $20^\circ$ to $30^\circ$ for various ratios of the deformation process.

3. Experimental studies on the distortion of the dividing grid confirm the rationality of the choice of the configuration of kinematic module 2 of a triangular shape with curvilinear borders. A comparative analysis of force regimes obtained theoretically and experimentally also confirms the viability of the developed estimation process scheme. The deviation of the data obtained on the basis of the proposed calculation scheme of the process from the experimentally obtained data on extrusion pressure does not exceed 13–15 %.

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