Multi-objective optimization of directed energy deposition process by using Taguchi-Grey relational analysis

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Abstract
In this study, a multi-objective optimization of directed energy deposition (DED) process was conducted with Taguchi-Grey relational analysis. The used part was designed as a flat rectangle which would be deposited by a single-layer and multi-track DED process. Firstly, after finishing Taguchi experiments, the effects of five control factors (laser power, overlap ratio, powder feed rate, scanning speed and laser defocus distance) on three DED product qualities (cladding efficiency, surface roughness and porosity) were, respectively, analyzed. Then, through Grey relational analysis (GRA), an optimal factor setting which can take all qualities into account was found and had better deposition results compared with previous setting. Furthermore, ANOVAs were conducted to find out significant factors of each qualities. By using the significant factors as variations, three second-order polynomial regression predictive models for qualities were created. Based on the GRA and ANOVAs results, additional one-factor-at-a-time (OFAT) experiments which used the optimal setting as the center point were performed. The qualities variation resulting from adjusting overlap ratio and laser defocus distance of optimal setting were investigated, and the results were also used as additional data to verified the accuracies of three regression models.

Keywords Directional energy deposition · Taguchi-Grey relational analysis · Cladding efficiency · Surface roughness · Porosity

1 Introduction
DED is a metal additive manufacturing technology. It uses powder feeding gas to transport metal powder to the energy center of heat source and the melted powder directly deposited on a substrate or surface of an unfinished part. By repeating the deposition layer by layer, a 3D product can be fabricated by DED.

Because of numerous advantages such as short production period, material saving, good mechanical properties of products and the ability to produce parts with complex geometry, DED frequently be used in various fields in recent years. However, DED has many control factors that can affect product qualities such as cladding efficiency, surface roughness and porosity. Above three qualities, respectively, have great influences on processing time and cost of manufacturing, products surface topography and products strength. So, to realize how factors affect qualities and to obtain better qualities which user need are the important research goals of DED field.

Kuriya et al. [1] pointed out that high energy input can prolong the solidification time melt pool requiring, thereby reducing the voids of products. Base on Liu et al. [2] research results, surface roughness increased if laser energy density was too high or too low. However, porosity rose sharply (>5%) when laser energy density was too high. It was considered resulting from that excessive energy caused thermal residual stress and made internal fractures. Li and Ma [3] established a model to simulate the cross section shape of single-layer and multi-track DED part, and revealed...
that surface roughness had an oscillating decrease as overlap ratio increased. Zhong et al. [4] mentioned that porosity decrease occurs with laser power increasing or powder feed rate decreasing. Deposition rate and powder usage ratio both increase with laser power increasing, but only deposition rate increases as powder feed rate increasing, powder usage ratio had an opposite trend. Scanning speed had no obvious effect on porosity, deposition rate and powder usage ratio. Gao et al. [5] adjusted laser defocus distance to conduct DED experiments; from the results, they found that when the laser defocus distance was set below the deposition surface, the laser energy distribution was more uniform and the qualities of deposited product was better. Ma et al. [6] proposed that the defocus was the most significant parameter on dilution which had nearly a linear effect. Zheng et al. [7] results show that the accumulation of un-melted powder particles on the side walls of deposited sections can be avoided by selecting a laser under-focused condition. In this study, laser defocus was chosen as one of the process parameters. Bhardwaj et al. [8] pointed out that the main challenge in laser deposition of metallic powders on a substrate is the selection of a suitable range of the involved process parameters. D.R. Feenstra et al. [9] results showed that laser power, scan speed and powder supply rate were the most influential parameters. Guo et al. [10] found that the laser power and overlap ratio are significant to the flatness ratio. Therefore, this study considered overlap ratio as our control factor as well.

In order to analyze the impacts of multiple factors on qualities more efficiently and comprehensively, many DoE methods which has been widely used in other fields [11–13] were gradually applied in DED researches. Ng et al. [14] used response surface methodology to conduct experiments and combined with ANOVAs to study the effects of process factors on the porosity of DED products. Qi et al. [15] selected the width and height of DED single-track product as the qualities to perform factors screening experiments and used central composite design method to design experiments. Found out significant factors and build regression model. Then used laser power to achieve the width control of single-track DED product and finished blade repairments. Lee et al. [16] investigated the effects of process parameters on deposited single-track geometry. The cross-sectional profile of the deposited bead was analyzed to understand the effects of each process condition on the bead geometry. Moreover, a mathematical formula for bead geometry prediction was derived using the RSM, which can be used to effectively control the process variables to achieve the desired qualities. Sheshadri et al. [17] conducted the Taguchi experiment determine optimal levels resulting in better surface quality and microhardness. Lian et al. [18] used Taguchi-Grey relational analysis to design experiments in order to optimize deposition rate and product surface flatness of single-layer multi-track DED products. The obtained optimal factor setting can simultaneously improve the two qualities.

After reviewing the research results mentioned above, it can be found that most scholars focused on the influences of factors on single quality and tried to figure out the mechanisms. However, it was rarely mentioned that how to adjust factor setting when multiple qualities of a DED product conflict with each other. Although Lian et al. [18] used Taguchi-Grey relational analysis to design and conduct multi-objective optimization research, their optimization targets only chose deposition rate and surface roughness. Cladding efficiency and porosity, which are closely related to the cost of powder materials and the mechanical strength of the products, are also extremely important qualities and need to be optimized.

So, the biggest goal of this research was finishing a multi-objective optimization by using Taguchi-Grey relational analysis as DoE method. Laser power, overlap ratio, powder feed rate, scanning speed and laser defocus distance were selected as the control factors of DoE in order to optimize cladding efficiency, surface roughness and porosity of DED products. The variation trends of each quality were investigated when the control factors were varied and the optimal factor setting which can simultaneously take the three qualities into account was found. ANOVAs were also conducted to find out significant factors of each qualities. By using the significant factors as variations, three second-order polynomial regression predictive models for qualities were built.

Furthermore, according to the GRA and ANOVAs results, two OFAT experiments which used the optimal setting as the center point were performed. Adjusted the overlap ratio and laser defocus distance of the optimal setting and investigated the three qualities variations. Then, the OFAT experiment results were used to verified the accuracies of three qualities regression models.

2 Materials and methods

2.1 Equipment and materials

IPG YLS-3000 fiber laser with 1070 nm wavelength and 3000 W maximum power was used in this research. The laser spot diameter was 3 mm, and it had a flat-top energy distribution. The used Precitec YC30 laser head was coaxial four-way powder feeding type and it had a hub which can used to adjust the laser focus position. GTV PF 2/2 LC powder feeder was used to transport metal powder to the laser head. It had a rotating powder disk and transporting unit was rpm. It was measured that 1 rpm was equivalent to 10.08 g/min. The laser head was installed on Tongtai TMV-710A...
machine tool which equipped with a double rotary table and can perform five-axis simultaneous movement.

The powder and substrates materials used in this study were both nickel-based superalloy IN 718. This alloy presents excellent properties at high-temperature applications (useful up to 980°C), oxidation, and corrosion-resistant properties, and it is widely used in the aeronautical sector [19]. The dimensions of the substrate were: L100 x W100 x H15 mm. The IN 718 powder was generated by gas atomization. The particle size distribution range of the powder was 53-150 μm. The composition of this powder is shown in Table 1.

2.2 Design of Taguchi experiment

Taguchi method is a multivariate experiment design method. Through mathematical and statistical tools, it helps researchers more effectively to study relations between multi-level control factors and product quality and find an optimal factor setting.

In order to fabricate solid products, firstly it is necessary to ensure the quality of single layer deposition. Therefore, this study used a flat rectangle as experiment product (as shown in Fig. 1), and chose laser power, overlap ratio, powder feed rate, scanning speed and laser defocus distance as control factors to design the Taguchi experiment. Optimized DED product qualities of single-layer and multi-track deposition process.

The definition of overlap ratio is shown below and in Fig. 2.

\[
\text{Overlap ratio} = \frac{W - H}{W} \times 100\% 
\]

where

\(W\): Width of single track

\(H\): Hatching space

The laser defocus distance means the relative distance between the laser focus \(F_L\) and deposition surface \(F_S\) under the premise that the positions of powder focus \(F_P\) and \(F_S\) are the same. As shown in Fig. 3, positive/negative refers to the position above/below \(F_S\) and the value refers to the distance.

In this Taguchi experiment, it was assumed that there was no strong interaction between the control factors. \(L_{16}\) orthogonal array was used to design the Taguchi experiment with five four-level control factors and it was repeated three times (as shown in Tables 2 and 3).

2.3 Product properties and Signal-to-Noise Ratio (SNR) criteria

Cladding efficiency, surface roughness and porosity were chosen as the optimization target qualities in this research. The definitions, calculation and measurement approaches of each quality are show below.
1 Cladding efficiency ($CE$) where $W_{\text{clad}}$: Increase of substrate weight after cladding. $W_{\text{feed}}$: Weight of input powder which is equal to the product of powder feed rate and cladding time.

The SNR conversion criterion of $CE$ was large-the-better (LTB). Its formula is:

$$CE = \frac{W_{\text{clad}}}{W_{\text{feed}}} \cdot 100\%$$

where $\eta_1$: SNR of cladding efficiency. $y_i$: Measurement value of $i$-th experiment. $n$: Experiment repeated times.

2 Surface roughness ($Sa$)

Bruker’s ContourGT-K white light interferometer was used to measure the surface roughness of top surface of deposited products. The used measurement criterion was arithmetic mean height of the surface ($Sa$). The SNR conversion criterion of $Sa$ was smaller-the-better (STB). Its formula is:

$$Sa = \frac{\sum_{i=1}^{n} y_i^2}{n}$$

where $\eta_2$: SNR of surface roughness.

3 Porosity ($P_t$)

After depositions, specimens were cut along the cross section of the parts by WEDM. Then, the specimens were grinded and polished with sandpaper and diamond slurry. Used Leica DM6000M optical microscope to take images of the specimens (at 7.5 magnification times), and the image analysis software Image J was used to calculate the area of pores in the specimen cross sections (as shown in Fig. 4).

The calculation formula of the porosity is shown in (2.3–2.4), and it also used small-the-better SNR conversion criterion.

$$P_t = \frac{\sum_{i=1}^{n} A_i}{A_c + A_M} \cdot 100\%$$

where $\sum_{i=1}^{n} A_i$: Sum of cross section area of pores. $A_c$: Cross section area of deposited material. $A_M$: Cross section area of melt pool.

Table 2 Control factors and its level values

| Notation | Factor                      | Level 1 | Level 2 | Level 3 | Level 4 |
|----------|-----------------------------|---------|---------|---------|---------|
| A        | Laser power (W)             | 800     | 1000    | 1200    | 1400    |
| B        | Overlap ratio (%)           | 30      | 40      | 50      | 60      |
| C        | Powder feed rate (rpm)      | 0.7     | 1       | 1.3     | 1.6     |
| D        | Scanning speed (mm/s)       | 4       | 7       | 10      | 13      |
| E        | Laser defocus distance (mm) | -2      | -1      | 0       | 1       |

Table 3 $L_{16}$ orthogonal array

|   | A Laser power (W) | B Overlap ratio (%) | C Powder feed rate (rpm) | D Scanning speed (mm/s) | E Laser defocus (mm) |
|---|-------------------|---------------------|--------------------------|-------------------------|----------------------|
| 1 | 800               | 30                  | 0.7                      | 4                       | -2                   |
| 2 | 800               | 40                  | 1                        | 7                       | -1                   |
| 3 | 800               | 50                  | 1.3                      | 10                      | 0                    |
| 4 | 800               | 60                  | 1.6                      | 13                      | 1                    |
| 5 | 1000              | 30                  | 1                        | 10                      | 1                    |
| 6 | 1000              | 40                  | 0.7                      | 13                      | 0                    |
| 7 | 1000              | 50                  | 1.6                      | 4                       | -1                   |
| 8 | 1000              | 60                  | 1.3                      | 7                       | -2                   |
| 9 | 1200              | 30                  | 1.3                      | 13                      | -1                   |
| 10| 1200              | 40                  | 1.6                      | 10                      | -2                   |
| 11| 1200              | 50                  | 0.7                      | 7                       | 1                    |
| 12| 1200              | 60                  | 1                        | 4                       | 0                    |
| 13| 1400              | 30                  | 1.6                      | 7                       | 0                    |
| 14| 1400              | 40                  | 1.3                      | 4                       | 1                    |
| 15| 1400              | 50                  | 1                        | 13                      | -2                   |
| 16| 1400              | 60                  | 0.7                      | 10                      | -1                   |
where \( \eta_3 \): SNR of porosity.

After finishing Taguchi experiments and SNRs analysis, ANOVAs were conducted to assess the effect levels of control factors on the three qualities, and found the most significant control factors. The significant factors were used as variables to create second-order polynomial regression models of three qualities.

### 2.4 Grey relational analysis

Taguchi method can optimize “one” quality and find the optimal factor setting. However, the DED optimization problem in this research is a “multi-objective” optimization problem. In order to take all qualities into account at the same time and try not to be biased, this research used Grey relational analysis (GRA) method based on Taguchi experiment to find the optimal factor setting. There are three steps in Grey relational analysis:

1. **Grey relation generating**
   The action of processing various data with different order levels and making them comparable is “Grey relation generation.” Considering the characteristic of SNR, the SNRs of three qualities were normalized to \([0,1]\). The normalization formula is shown in Eq. 6. Figure 5 shows the procedure diagram of GRA.

2. **Grey relational coefficient (GRC) calculation**
   Then convert the normalized SNRs into the Grey correlation coefficient.

3. **Grey relational grade (GRG) calculation**
   Finally, the three GRCs were integrated as GRG with the same weight value.

After the above three steps, three SNRs were integrated as one GRG. Then, it could follow Taguchi method to analyze the control factors and find the optimal factor setting.

### 3 Results and discussion

After three repeated Taguchi experiments, the images of some deposited products are shown in Fig. 6. The average Taguchi experiment results and the converted SNR are shown in Table 4:

#### 3.1 Cladding efficiency

Table 5 and Fig. 7 which were made by the cladding efficiency SNR \( (\eta_1) \) data of Table 4 show the effect levels on \( \eta_1 \) of control factors.
As shown in Table 5, the effect level order of factors is: powder feed rate (C) > laser power (A) > laser defocus distance (E) > overlap ratio (B) > scanning speed (D). According to the levels which each factor can get the highest \( \eta_1 \), the optimal factor setting that can get the best deposition efficiency is: A_4 B_1 C_1 D_3 E_1.

In Fig. 7, \( \eta_1 \) increases when laser power and scanning speed increase. The reasons are listed following. (1) The laser power increase makes the input powder more likely to be melt and deposited. (2) The scanning speed increase has a greater effect on reduction of powder input per unit time. However, this study used the concept of powder usage to define the cladding efficiency; the reduction of powder input amount will relatively increase the percentage of powder which can be melt by constant laser power. So, the cladding efficiency increases as scanning speed increases.

In addition, \( \eta_1 \) decreases when overlap ratio, powder feed rate and laser defocus distance increase. The reasons are listed following. (1) The larger overlap ratio the smaller the hatching space. It will increase the probability of powder hitting old tracks and rebounding. (2) The powder that can be melt by the laser is limited, and the excessive powder is difficult to be melt and used, which resulting in lower cladding efficiency. (3) As the study of Gao et al. [5], when Gaussian laser is set at negative defocus position, the energy distribution of the beam spot section is relatively even. This phenomenon should be the same in the flat-top laser used in this study. Then, when the laser defocus distance increases from negative to positive, the energy density at the edge of the spot decreases sharply and reduce the percentage of powder usage.

### 3.2 Surface roughness

Table 6 and Fig. 8 which were made by the surface roughness SNR (\( \eta_2 \)) data of Table 4 show the effect levels on \( \eta_2 \) of control factors.

As shown in Table 6, the effect level order of factors is: scanning speed (D) > powder feed rate (C) > overlap ratio (B) > laser power (A) > laser defocus distance (E). According to the levels which each factor can get the highest \( \eta_2 \), the optimal factor setting that can get the best surface roughness is: A_2 B_4 C_2 D_4 E_3.

In Fig. 8, \( \eta_2 \) increases when overlap ratio and scanning speed increase and decreases when powder feed rate increases. However, when the laser power and laser defocus distance increase, the value of \( \eta_2 \) oscillates in a small range without significant change.

The variation trend that surface roughness becomes better when overlap ratio increase is consistent with the research results of Li and Ma [3]. When the powder feed rate increases, if input powder be deposited successfully, the single track will have a larger aspect ratio and contact angle. This characteristic will result in a rough top surface of product when the single tracks overlap track by track. By contrast, the scanning speed increases will reduce the amount of powder input per unit time and lets the single track with a low aspect ratio. So, its multi-track product will have better surface roughness.

### 3.3 Porosity

Table 7 and Fig. 9 which were made by the porosity SNR (\( \eta_3 \)) data of Table 4 show the effect levels on \( \eta_3 \) of control factors.

As shown in Table 7, the effect level order of factors is: laser power (A) > laser defocus distance (E) > powder feed rate (C) > scanning speed (D) > overlap ratio (B). According to the levels which each factor can get the highest \( \eta_3 \), the optimal factor setting that can get the lowest porosity is: A_4 B_4 C_1 D_1 E_4.
Table 4 Qualities and SNRs of Taguchi experiment products

| Run | A     | B     | C     | D     | E     | Cladding efficiency (%) | Surface roughness (μm) | Porosity (%) | SNR  |
|-----|-------|-------|-------|-------|-------|--------------------------|------------------------|--------------|------|
|     | Laser power (W) | Overlap ratio (%) | Powder feed rate (rpm) | Scanning speed (mm/s) | Laser defocus (mm) | Cladding efficiency | Surface roughness | Porosity | SNR  |
| 1   | 800   | 30    | 0.7   | 4     | −2    | 57.26%                   | 47.82                  | 0.34%        | −4.893 | −33.622 | 49.265 |
| 2   | 800   | 40    | 1     | 7     | −1    | 44.64%                   | 29.98                  | 0.35%        | −7.224 | −29.583 | 49.059 |
| 3   | 800   | 50    | 1.3   | 10    | 0     | 41.55%                   | 32.06                  | 0.43%        | −7.640 | −30.270 | 47.186 |
| 4   | 800   | 60    | 1.6   | 13    | 1     | 33.79%                   | 22.65                  | 0.28%        | −9.426 | −27.361 | 51.085 |
| 5   | 1000  | 30    | 1     | 10    | 1     | 43.93%                   | 28.16                  | 0.24%        | −7.228 | −29.053 | 52.339 |
| 6   | 1000  | 40    | 0.7   | 13    | 0     | 54.12%                   | 20.46                  | 0.23%        | −5.476 | −26.279 | 52.575 |
| 7   | 1000  | 50    | 1.6   | 4     | −1    | 36.58%                   | 44.81                  | 0.21%        | −8.789 | −33.032 | 53.484 |
| 8   | 1000  | 60    | 1.3   | 7     | −2    | 45.07%                   | 35.20                  | 0.35%        | −6.977 | −30.945 | 49.079 |
| 9   | 1200  | 30    | 1.3   | 13    | −1    | 55.39%                   | 34.74                  | 0.48%        | −5.137 | −31.335 | 46.206 |
| 10  | 1200  | 40    | 1.6   | 10    | −2    | 55.29%                   | 31.17                  | 0.39%        | −5.164 | −30.103 | 47.496 |
| 11  | 1200  | 50    | 0.7   | 7     | 1     | 53.94%                   | 28.75                  | 0.10%        | −5.438 | −29.628 | 59.651 |
| 12  | 1200  | 60    | 1     | 4     | 0     | 45.92%                   | 35.13                  | 0.12%        | −6.782 | −30.964 | 57.259 |
| 13  | 1400  | 30    | 1.6   | 7     | 0     | 47.74%                   | 39.18                  | 0.14%        | −6.424 | −31.932 | 56.452 |
| 14  | 1400  | 40    | 1.3   | 4     | 1     | 50.98%                   | 54.48                  | 0.11%        | −6.095 | −34.813 | 58.446 |
| 15  | 1400  | 50    | 1     | 13    | −2    | 64.48%                   | 22.76                  | 0.25%        | −3.833 | −27.275 | 51.654 |
| 16  | 1400  | 60    | 0.7   | 10    | −1    | 66.43%                   | 24.56                  | 0.08%        | −3.608 | −28.147 | 60.487 |
In Fig. 9, $\eta_3$ increases when laser power, overlap ratio and laser defocus distance increase. The reasons are listed following. (1) Increasing laser power can melt powder more completely. According to Tatsuhiko Kuriya et al. research [1], a larger amount of heat prolongs the solidification time of melt pool, allowing the bubbles to escape and reducing the porosity of the product. (2) In addition, a higher overlap ratio means that the hatching space between the tracks is short. The old deposited track will continue to be affected by the heat of the new track, and it will also increase the probability of bubbles escaping. (3) Because laser energy at the positive defocus will be more concentrated in the center [3], it leads to a higher temperature and prolong the time for the bubbles to leave.

Besides, $\eta_3$ decreases when powder feed rate and scanning speed increase. The reasons are listed following. (1) The more powder input, the more laser energy will be dispersed. It will cause the temperature of the overall deposit to drop and reduce the time required for solidification. It results in more air bubbles in products.

### 3.4 ANOVA results of properties

The ANOVA results of cladding efficiency SNR ($\eta_1$) are shown in Table 8. In this study, one-half rule was used, which selects the first three control factors having the highest contribution to the variation of $\eta_1$ as significant factors. Then, the overlap ratio (B) and scanning speed (D) which had lower effect level were pooled as the experiment error to calculate F-values and confidence levels.

The confidence levels for the significance of laser power (A), powder feed rate (C) and laser defocus distance (E) are 98.86%, 98.53% and 94.16%, respectively, showing that these three factors have significant influences on $\eta_1$ variation. Their contributions of to the $\eta_1$ variation are 38.58%, 34.73% and 18.35%. Compared with the experiment error (pooled B and D factors), which accounts for 8.34%, A, C and E factors have significant effects on cladding efficiency.

The ANOVA results of surface roughness SNR ($\eta_2$) are shown in Table 9. Similarly, one-half rule was used, and the laser power (A) and laser defocus distance (E) were pooled as the experiment error to calculate F-values and confidence levels.

The confidence levels for the significance of overlap ratio (B), powder feed rate (C) and scanning speed (D) are 98.26%, 99.62 and 99.98%, respectively, showing that these three factors have significant influences on $\eta_2$ variation. Their contributions of to the $\eta_2$ variation are 11.21%, 20.85% and 65.05%. Compared with the experiment error (pooled A and E factors), which accounts for 2.89%, B, C and D factors have significant effects on surface roughness.

The ANOVA results of porosity SNR ($\eta_3$) are shown in Table 10. Since the effects of the five factors on $\eta_3$ are closer, only the overlap ratio (B) which has the lowest significance was pooled as the experiment error to calculate the F-value and confidence levels.

### Table 5 The average cladding efficiency SNR ($\bar{n}_1$) obtained at the condition of F factor and K level

|        | A   | B   | C   | D   | E   |
|--------|-----|-----|-----|-----|-----|
| Level 1| -7.296 | -5.920 | -4.854 | -6.640 | -5.217 |
| Level 2| -7.117 | -5.990 | -6.267 | -6.516 | -6.189 |
| Level 3| -5.630 | -6.425 | -6.462 | -5.910 | -6.580 |
| Level 4| -4.990 | -6.698 | -7.451 | -5.968 | -7.047 |
| Range  | 2.306 | 0.778 | 2.597 | 0.730 | 1.830 |

### Table 6 The average surface roughness SNR ($\bar{n}_2$) obtained at the condition of F factor and K level

|        | A   | B   | C   | D   | E   |
|--------|-----|-----|-----|-----|-----|
| Level 1| -30.21 | -31.49 | -29.42 | -33.11 | -30.49 |
| Level 2| -29.83 | -30.19 | -29.22 | -30.52 | -30.52 |
| Level 3| -30.51 | -30.05 | -31.84 | -29.39 | -29.86 |
| Level 4| -30.54 | -29.35 | -30.61 | -28.06 | -30.21 |
| Range  | 0.714 | 2.131 | 2.622 | 5.045 | 0.663 |

Fig. 7 Response graph of cladding efficiency SNR ($\eta_1$)
The confidence levels for the significance of laser power (A), powder feed rate (C), scanning speed (D) and laser defocus distance (E) are 94.54%, 80.82%, 71.38% and 87.49%, respectively, showing that these four factors have significant influences on \( \eta_2 \) variation. Their contributions of to the \( \eta_2 \) variation are 37.31%, 17.83%, 13.08% and 23.59%. Compared with the experiment error (pooled B factors), which accounts for 8.19%, A, C, D and E factors have significant effects on porosity.

The confidence levels for the significance of laser power (A), powder feed rate (C), scanning speed (D) and laser defocus distance (E) are 94.54%, 80.82%, 71.38% and 87.49%, respectively, showing that these four factors have significant influences on \( \eta_3 \) variation. Their contributions of to the \( \eta_3 \) variation are 37.31%, 17.83%, 13.08% and 23.59%. Compared with the experiment error (pooled B factors), which accounts for 8.19%, A, C, D and E factors have significant effects on porosity.
3.5 Regression models

Based on the results of ANOVAs, this study took the significant factors of each quality as variables, and established a second-order polynomial regression model. However, the units and magnitudes of levels of these factors were not the same. Before building the regression model, the levels of control factors were all normalized to $[-1,1]$, but their respective distributions of level values were still the same.

$$\text{Un}_{\text{FK}} = \frac{U_{\text{FK}} - \mu_F}{\text{Max}(U_{\text{FK}}) - \text{Min}(U_{\text{FK}})} \in [-1,1] \quad (10)$$

where $U_{\text{Na,FK}}$: Normalized i-th level of a control factor, $U_{\text{FK}}$: The i-th level of a control factor before normalization, $\mu_F$: Average of level values of a control factor.

Table 11 shows $L_{16}$ array with normalization control factors and the average measurement value of qualities.

The following are the regression prediction equations of the three qualities.

$$S_a = 31.61 - 7.86 \cdot B + 6.68 \cdot C - 19.66 \cdot D - 6.35 \cdot B \cdot C + 10.34 \cdot B \cdot D - 0.88 \cdot C \cdot D + 2.11 \cdot B^2 - 12.54 \cdot C^2 + 22.17 \cdot D^2 \quad (12)$$

$$P_t = 0.3084 - 0.2186 \cdot A + 0.1459 \cdot C + 0.2661 \cdot D - 0.094 \cdot E + 0.0212 \cdot A \cdot C + 0.1865 \cdot A \cdot D + 0.4765 \cdot A \cdot E + 0.2216 \cdot C \cdot D - 0.0609 \cdot C \cdot E - 0.22 \cdot D \cdot E - 0.0712 \cdot A^2 - 0.2089 \cdot C^2 - 0.0941 \cdot E^2 \quad (13)$$

The $R^2$ values of regression models of cladding efficiency and surface roughness are 0.9105 and 0.8806. It means that the regression models using the significant control factors of the two qualities as the variables have good ability to present the experiment results. So, the two regression models can be used to primarily predict cladding efficiency and surface roughness of DED products.

The $R^2$ value of porosity regression model which is created by using four control factors as variables is 0.9745. It means that the porosity model has great ability to present the experiment results. However, the extremely high $R^2$ of this model may also be caused by the model overfitting. Because there were four variables used to build porosity regression model (the others have three variables), only 16 pieces of data obtained from $L_{16}$ experiment may be not enough. To

| Factor | SS   | DOF | Var  | F-Value | Confidence level | Contribution |
|--------|------|-----|------|---------|-----------------|--------------|
| A      | 119.003 | 3   | 39.668 | 4.553   | 94.54%          | 37.31%       |
| B      | Pooled |     |       |         |                 |              |
| C      | 56.880  | 3   | 18.960 | 2.176   | 80.82%          | 17.83%       |
| D      | 41.709  | 3   | 13.903 | 1.596   | 71.38%          | 13.08%       |
| E      | 75.261  | 3   | 25.087 | 2.880   | 87.49%          | 23.59%       |
| Error  | 26.135  | 3   | 8.712  |         |                 | 8.19%        |
| Total  | 318.988 | 15  | -     | -       |                 | 100%         |
confirm whether there is an overfitting problem, it needs to test the model with additional experiment data. Therefore, this study used additional experiment data to test the predictive abilities of cladding efficiency and surface roughness regression models and whether there is an overfitting problem in porosity model. This part will be presented and discussed in Sect. 4.3.

### 3.6 Grey relational analysis

In 3.1–3.3 sections, the analysis results of Taguchi experiment show that the optimal factor settings of cladding efficiency, surface roughness and porosity are $A_4 B_1 C_1 D_3 E_1$, $A_2 B_4 C_2 D_4 E_3$ and $A_4 B_4 C_1 D_1 E_4$, respectively. Obviously, the optimal settings of each quality are not

| Run | Laser power, A | Overlap ratio, B | Powder feed rate, C | Scanning speed, D | Laser defocus distance, E | Average CE (%) | Average $S_a$(µm) | Average $P_t$ (%) |
|-----|----------------|-----------------|---------------------|-------------------|--------------------------|---------------|-----------------|-----------------|
| 1   | −0.500         | −0.500          | −0.500              | −0.500            | −0.500                   | 57.26%        | 47.82           | 0.34%           |
| 2   | −0.500         | −0.167          | −0.167              | −0.167            | 0.167                    | 44.64%        | 29.98           | 0.35%           |
| 3   | −0.500         | 0.167           | 0.167               | 0.167             | 0.500                    | 41.55%        | 32.06           | 0.43%           |
| 4   | −0.500         | 0.500           | 0.500               | 0.500             | 0.500                    | 33.79%        | 22.65           | 0.28%           |
| 5   | −0.167         | −0.500          | −0.167              | 0.167             | 0.500                    | 43.93%        | 28.16           | 0.24%           |
| 6   | −0.167         | −0.167          | −0.500              | 0.500             | 0.167                    | 54.12%        | 20.46           | 0.23%           |
| 7   | −0.167         | 0.167           | 0.500               | −0.500            | −0.167                   | 36.58%        | 44.81           | 0.21%           |
| 8   | −0.167         | 0.500           | 0.167               | −0.167            | −0.500                   | 40.07%        | 35.20           | 0.35%           |
| 9   | 0.167          | −0.500          | 0.167               | −0.167            | −0.500                   | 55.39%        | 34.74           | 0.48%           |
| 10  | 0.167          | −0.167          | 0.500               | 0.167             | 0.500                    | 53.94%        | 31.17           | 0.39%           |
| 11  | 0.167          | 0.167           | −0.500              | 0.500             | −0.167                   | 45.92%        | 35.13           | 0.12%           |
| 12  | 0.167          | 0.500           | −0.167              | −0.500            | 0.167                    | 47.74%        | 39.18           | 0.14%           |
| 13  | 0.500          | −0.500          | 0.500               | −0.167            | 0.500                    | 52.339        | 50.98%          | 0.11%           |
| 14  | 0.500          | −0.167          | 0.500               | 0.167             | 0.500                    | 53.94%        | 44.81           | 0.21%           |
| 15  | 0.500          | 0.167           | −0.500              | 0.500             | 0.500                    | 53.94%        | 28.75           | 0.10%           |
| 16  | 0.500          | 0.500           | −0.500              | 0.500             | −0.500                   | 54.12%        | 20.46           | 0.23%           |

### Table 12 $L_{16}$array showing GRA data processing procedures

| Run | S/N ratio | Normalization of S/N ratio | GRC | GRG |
|-----|-----------|-----------------------------|-----|-----|
| 1   | −4.893    | −33.622                     | 49.265 | 0.779 | 0.140 | 0.214 | 0.694 | 0.368 | 0.389 | 0.483 |
| 2   | −7.224    | −29.583                     | 49.059 | 0.379 | 0.613 | 0.200 | 0.446 | 0.564 | 0.385 | 0.464 |
| 3   | −7.640    | −30.270                     | 47.186 | 0.307 | 0.532 | 0.069 | 0.419 | 0.517 | 0.349 | 0.42  |
| 4   | −9.426    | −27.361                     | 51.085 | 0.000 | 0.873 | 0.342 | 0.333 | 0.798 | 0.432 | 0.520 |
| 5   | −7.228    | −29.053                     | 52.339 | 0.378 | 0.675 | 0.429 | 0.446 | 0.606 | 0.467 | 0.506 |
| 6   | −5.476    | −26.279                     | 52.575 | 0.679 | 1.000 | 0.446 | 0.609 | 1.000 | 0.474 | 0.694 |
| 7   | −8.789    | −33.032                     | 53.484 | 0.109 | 0.209 | 0.510 | 0.360 | 0.387 | 0.505 | 0.417 |
| 8   | −6.977    | −30.945                     | 49.079 | 0.421 | 0.453 | 0.201 | 0.463 | 0.478 | 0.385 | 0.442 |
| 9   | −5.137    | −31.335                     | 46.206 | 0.737 | 0.408 | 0.000 | 0.655 | 0.458 | 0.333 | 0.482 |
| 10  | −5.164    | −30.103                     | 47.496 | 0.733 | 0.552 | 0.090 | 0.652 | 0.527 | 0.355 | 0.511 |
| 11  | −5.438    | −29.628                     | 59.651 | 0.685 | 0.608 | 0.941 | 0.614 | 0.560 | 0.895 | 0.689 |
| 12  | −6.782    | −30.964                     | 57.259 | 0.454 | 0.451 | 0.774 | 0.478 | 0.477 | 0.689 | 0.547 |
| 13  | −6.424    | −31.932                     | 56.452 | 0.516 | 0.338 | 0.717 | 0.508 | 0.430 | 0.639 | 0.525 |
| 14  | −6.095    | −34.813                     | 58.446 | 0.573 | 0.000 | 0.857 | 0.539 | 0.333 | 0.778 | 0.549 |
| 15  | −3.833    | −27.275                     | 51.654 | 0.961 | 0.883 | 0.381 | 0.928 | 0.811 | 0.447 | 0.728 |
| 16  | −3.608    | −28.147                     | 60.487 | 1.000 | 0.781 | 1.000 | 1.000 | 0.696 | 1.000 | 0.898 |

Max \(-3.608\) \(-26.279\) \(60.487\) - - - Avg. (\(R\)) 0.555

Min \(-9.426\) \(-34.813\) \(46.206\) - - -
the same, and variation trends caused by a control factor for different qualities are even opposite. Therefore, this study based on the Taguchi experiment data, used Grey relational analysis to help to achieve the goal of simultaneously optimizing the three qualities. As mentioned in Sect. 2.4, the Grey relational analysis is divided into three steps to process the SNRs and convert the “three” qualities into “one” composite index (Grey relational grade, GRG). So, the DED process quality can be comprehensively evaluated and the optimal factor setting for all qualities can be determined.

After calculating the GRG (as shown in Table 12), the study followed Taguchi’s method again to make a factor response graph to analyze the effects of control factors on the variation of GRG.

As shown in Fig. 10 and Table 13, the effect level order of factors is: powder feed rate (C) > laser power (A) > scanning speed (D) > laser defocus distance (E) > overlap ratio (B). According to the levels which each factor can get the highest R, the optimal factor setting that can get the highest GRG is: A₄ B₄ C₁ D₄ E₄.

Similarly, this study also performed an ANOVA for GRG (the results are shown in Table 14). the degree of overlap B and the laser defocus distance E, which have a less obvious impact on the variance of R, are combined (Pooled) as the experimental error (Error). The overlap ratio (B) and laser defocus distance (E) which had lower effect level were pooled as the experiment error.

The laser power (A), powder feed rate (C) and scanning speed (D) are the significant factors of which confidence levels for the significance are 98.22%, 98.98% and 83.96%, respectively. Their contributions to the R variation are 38.12%, 44.44% and 11.27%.

### 4 Verification and one-factor-at-a-time experiments

#### 4.1 Verification of optimized factor setting

After finishing Taguchi-Grey relational analysis and obtaining the optimal factor setting (A₄ B₄ C₁ D₄ E₄), in order to verify the effectiveness of it, this study used it to deposit the 20×10 mm² flat rectangle product again and compared its deposition result with the one which is deposited by using laboratory previous setting for a thin-walled cylinder part. (laser power (A) 1000 W, powder supply (C) 1.1 rpm, scanning speed (D) 7 mm/s and laser defocus distance (E) −2 mm) In addition, the overlap ratio (B) was set as 60% which was equal to the optimal factor setting.

The two settings were deposited once, respectively, and the comparisons between their deposition results are shown as following. (Due to COVID-19 epidemic, the verification experiment used Nikon 10x optical microscope to take cross-sectional images as shown in Fig. 11.)

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**Table 13** The GRG obtained at the condition of F factor and K level

| A  | B  | C  | D  | E  |
|----|----|----|----|----|
| Level 1 | 0.474 | 0.499 | 0.691 | 0.499 | 0.541 |
| Level 2 | 0.514 | 0.555 | 0.561 | 0.530 | 0.565 |
| Level 3 | 0.557 | 0.565 | 0.475 | 0.585 | 0.549 |
| Level 4 | 0.675 | 0.602 | 0.493 | 0.606 | 0.566 |
| Range | 0.201 | 0.103 | 0.216 | 0.107 | 0.025 |

**Table 14** The ANOVA results of R

| Factor | SS  | DOF | Var  | F    | Confidence level | Contribution |
|--------|-----|-----|------|------|-----------------|--------------|
| A      | 0.091 | 3 | 0.030 | 7.662 | 98.22%           | 35.12%       |
| B      | Pooled |  |  |      |                 |              |
| C      | 0.115 | 3 | 0.038 | 9.697 | 98.98%           | 44.44%       |
| D      | 0.029 | 3 | 0.010 | 2.460 | 83.96%           | 11.27%       |
| E      | Pooled |  |  |      |                 |              |
| Error  | 0.024 | 6 | 0.004 | -    | -                | 9.17%        |
| Total  | 0.258 | 15 | -    | -    | 100%            |              |
It can be seen from the above comparison results shown in Table 15. The optimal setting \( A_4 B_4 C_1 D_4 E_4 \) had better qualities of DED product compared with the previous setting. It shows that the new factor setting can effectively improve the product qualities of the DED process in single-layer multi-track deposition.

### 4.2 One-factor-at-a-time experiment results

This study found an optimal factor setting \( A_4 B_4 C_1 D_4 E_4 \) for a single-layer and multi-track DED process that can take three qualities into account. However, 3D parts need to be stacked with multiple layers and often have different appropriate deposition toolpaths for different part geometries. They are the problems that the optimal factor setting for general single-layer and multi-track deposition need to face.

The overlap ratio (B) and laser defocus distance (E) are the most change-demanding control factors. The overlap ratio has a directly influence on the time span required for a part to be deposited. According to the literature review and laboratory past research [20], when the laser defocus distance is an appropriate negative value, the laser focus will provide a self-repairing function to eliminate the uneven surface of last layer. It is due to when the laser focus on negative defocus position passes through uneven surface, the focus will close to lower positions and away from higher positions.

Therefore, based on the ANOVA results of the GRG, the study adjusted the overlap ratio (B) and laser defocus distance (E) to conduct an one-factor-at-a-time (OFAT) experiment. The OFAT experiment did not change the significant factors, maintaining the level of laser power (A), powder feed rate (C) and scanning speed (D) at \( A_4 C_1 D_4 \). Similarly, using flat rectangle as experiment product, observed the variation trends of product qualities. Expecting when the significant factors were fixed, the quality variations caused by adjusting the overlap ratio and laser defocus distance will not be severe. So, the factor setting can flexibly adjust the two factors depending on different fabrication requirements. Using \( A_4 B_4 C_1 D_4 E_4 \) as the center setting, the OFAT experiment results are shown in Table 16.

It can be seen from the above OFAT experiment results (as shown in Figs. 12, 13 and 14) that except for the cladding efficiency having greater variation, the effects of adjusting overlap ratio and laser defocus distance on the surface roughness and porosity is relatively insignificant, both values oscillating in a small range. The variation trend of the cladding efficiency in the OFAT experiment is also the same as the analysis result in Sect. 3.1, which when the overlap ratio and laser defocus distance increase, the cladding efficiency has decreasing trends.

Combining the results of OFAT experiment and laboratory past research, the laser defocus distance is

### Table 15 Qualities comparison results of the verification experiment

|         | Cladding efficiency | Surface roughness | Porosity |
|---------|--------------------|------------------|----------|
|         | CE (%)   | \( n_1 \) | \( S_{\text{av}} \) (\( \mu \text{m} \)) | \( n_2 \) | \( P_t \) (%) | \( n_3 \) |
| Optimized setting | 61.41% | -4.235 | 13.99 | -22.916 | 0.036% | 68.938 |
| Previous setting | 47.35% | -6.494 | 30.34 | -29.640 | 0.088% | 61.096 |
Table 16 Results of OFAT experiment

| Run | Laser power (W) | Overlap ratio (%) | Powder feed rate (rpm) | Scanning speed (mm/s) | Laser defocus distance (mm) | Cladding efficiency (%) | Surface roughness (µm) | Porosity (%) |
|-----|-----------------|-------------------|------------------------|-----------------------|----------------------------|------------------------|-----------------------|-------------|
| 1   | 1400            | 60                | 0.7                    | 13                    | 1                          | 61.41%                 | 13.99                 | 0.036%      |
| 2   | 1400            | 50                | 0.7                    | 13                    | 1                          | 65.64%                 | 20.09                 | 0.025%      |
| 3   | 1400            | 40                | 0.7                    | 13                    | 1                          | 73.70%                 | 15.90                 | 0.025%      |
| 4   | 1400            | 30                | 0.7                    | 13                    | 1                          | 69.09%                 | 21.63                 | 0.040%      |
| 5   | 1400            | 60                | 0.7                    | 13                    | 0                          | 55.27%                 | 22.44                 | 0.060%      |
| 6   | 1400            | 60                | 0.7                    | 13                    | −1                         | 62.18%                 | 13.57                 | 0.078%      |
| 7   | 1400            | 60                | 0.7                    | 13                    | −2                         | 76.00%                 | 16.47                 | 0.039%      |

Fig. 12 Variation trends of cladding efficiency under adjusting a overlap ratio and b laser defocus distance

Fig. 13 Variation trends of surface roughness under adjusting a overlap ratio and b laser defocus distance

Fig. 14 Variation trends of porosity under adjusting a overlap ratio and b laser defocus distance
recommended to set as −2 mm (E1) based on cladding efficiency and the overlap degree was set as 30% (B1). So, the setting $A_4 B_1 C_1 D_4 E_1$ can maintain high cladding efficiency and low processing time.

### 4.3 Verifications of Regression Models

As mentioned in Sect. 3.5, additional experiment data are needed for comparison in order to know the predictive ability of qualities regression models. Therefore, this study compared the OFAT and verification experiment results with the predictive values of the regression models. The results are shown in Table 17. Since the regression models of cladding efficiency and porosity did not use the overlap ratio (B) as variable, the predicted values of the OFAT experiment runs using overlap ratio as independent variable were all the same. In the same way, the surface roughness model had a constant predictive value for the runs that used the laser defocus distance (E) as the independent variable in the OFAT experiment.

In Table 17, the average error between the predictive and experiment values of cladding efficiency is 9.98%, which can be said that the cladding efficiency regression model has good prediction accuracy. The average predictive error of the surface roughness model is 24.22%. The errors between predictive experiment values of each run are oscillating and the variation of predictive values is small. This shows that the predictive surface roughness has stabilized in this interval, but its oscillation amplitude is smaller than the actual measured value. Although not as accurate as the cladding efficiency model, this surface roughness model can still provide a predictive value as a reference when adjusting process factors.

The average predictive error of the porosity regression model is a very large value, 358%. It can be said that the accuracy of the prediction of the porosity model is not satisfactory. Comparing with its 0.9745 $R^2$ value, the “model overfitting” problem mentioned in Sect. 3.5 is revealed.

From the ANOVA results of porosity in Sect. 3.4, except for the laser power, the difference in effects of the other four factors on the porosity variation are not obvious. It means that these four factors may have similar significance and no one can be discarded. However, the Taguchi $L_{16}$ array can only produce 16 data. If use five factors for quadratic polynomial regression, the correct regression equation cannot be obtained due to insufficient simultaneous equations.

When draw the predictive and OFAT experiment values of porosity in the same line graph (as shown in Fig. 15), it can be observed that they have a similar variation trends during independent variables changing. Therefore, whether the experiment data are sufficient should be considered to avoid model overfitting problem. Then, the regression approach can have better prediction ability.
5 Conclusion

In this study, Taguchi $L_{16}$ array was used to design the five four-level factor deposition experiments, and three product qualities were obtained and converted into SNR for factor response analyses and ANOVAs. In addition, a one-factor experiment was used to further explore the non-significant factors and verify the accuracy of the model. The final analysis results came to the following conclusions:

(1) According to the analysis results, the most significant factors of cladding efficiency were: laser power, powder feed rate and laser defocus distance. The cladding efficiency increased when the laser power increased and decreased when the powder feed rate and laser defocus distance increased.

(2) The factors that had the most significant effect on the surface roughness were: the overlap ratio, powder feed rate and scanning speed. The surface roughness became better when the overlap ratio and scanning speed increased, and got worse when powder feed rate increased.

(3) The porosity was significantly affected by the laser power; however, the difference between the significances of the other four factors were not very obvious. Therefore, only the overlap ratio which had the lowest significance was considered as insignificant factor. The porosity decreased with the laser power and laser defocus distance increasing and increased with the powder feed rate and scanning speed increasing.

(4) Using Grey relational analysis to combine the three qualities into the Grey relational grade (GRG) and used it as a composite index to find the optimal factor setting: $A_4 B_4 C_1 D_4 E_1$. The results of ANOVA for the GRG showed that the laser power, powder supply and scanning speed were the most significant factors.

(5) In order to realize the flexibility and stability of optimal setting when it faces with different DED process applications, this study additionally used the overlap ratio and laser defocus distance as the independent variables to conduct the OFAT experiment. As its results, when adjusted the two factors, besides that the cladding efficiency had large variation, both the values of surface roughness and porosity oscillated in a small range. Therefore, considering cladding efficiency and processing time, this study recommended to use $A_4 B_1 C_1 D_4 E_1$ as the main factor setting and apply it to workpiece manufacturing in future path planning research.

(6) The Taguchi experiment data were used to build the regression models of three qualities by using their significant factors as variables. After comparing the experiment values obtained from the OFAT experiment, the results showed that the cladding efficiency and surface roughness regression model both had predictive capabilities. They were sufficient to be used as a tool for preliminary prediction of product quality.

(7) The porosity model had big error between its predictive and experiment values due to model over fitting problem. It was necessary to increase the number of samples to increase the accuracy of the regression model.

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Declarations

Ethics approval  The authors confirm the novelty of the reported work and confirm that it is not submitted to any other journal.

Consent to participate  The authors give consent to participate.

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