Empirical evidence that disease prevalence may affect the performance of diagnostic tests with an implicit threshold: a cross-sectional study

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ABSTRACT

Objective: To investigate the effects that prevalence has on the diagnostic performance of junior doctors in interpreting x-rays.

Design: Two-armed cross-sectional design using systematic sampling.

Setting: Emergency department in the UK.

Participants: From a sample of 2593 patients (1434 men and 1159 women) taken from an unselected attending cohort between January and April 2002, 967 x-rays were analysed. The sex distribution was 558 men and 409 women, and the mean age of those receiving an x-ray was 34.6.

Interventions: The interpretation of x-rays by junior doctors after their triage into high- and low-prevalence populations by radiographers.

Main outcome measures: Sensitivity, specificity, likelihood ratios, diagnostic odds ratios and receiver operator characteristic curve.

Results: There were statistically significant differences in the performance characteristics of junior doctors when interpreting high-probability and low-probability x-rays. For the high- and low-probability populations, respectively, the sensitivities were 95.8% (95% CI 91.1% to 98.1%) and 78.3% (95% CI 65.7% to 87.2%) and the specificities were 56.0% (95% CI 41.9% to 69.2%) and 92.3% (95% CI 90.0% to 94.2%). Hierarchical logistic regression showed that the sensitivity did depend on the type of x-ray being interpreted but the diagnostic odds ratios did not vary significantly with prevalence, suggesting that doctors were changing their implicit threshold between the two populations along a common receiver operator characteristic curve.

Conclusions: This study provides evidence on how the prevalence may affect the performance of diagnostic tests with an implicit threshold and potentially includes the clinical history and examination. This has implications both for clinicians applying research findings to their practice and the design of future studies.

INTRODUCTION

It is convenient in the assessment of diagnostic tests to divide the study population into two disjoint subpopulations consisting of those with disease and those without. Leading from this observation, many authors have asserted that performance characteristics, such as the sensitivity and specificity, which are derived from one or other of these...
THE EFFECT OF PREVALENCE ON THE SENSITIVITY AND SPECIFICITY OF A DIAGNOSTIC TEST

Between January and April 2002, systematic sampling was used to collect data on an unselected attending cohort of patients at the ED of the Horton Hospital in the UK. All patients seeing an ED junior doctor underwent a clinical examination to determine whether treatment or further investigation was necessary. As part of their evaluation, some patients were required to have an x-ray, where the type of x-ray received depended on the results of the clinical examination. Before the junior doctors viewed any x-rays, they were first interpreted then triaged, on the basis of their findings, by one of the departmental radiographers (radiologic technologists). Thus, those x-rays considered abnormal or ‘high-probability’ x-rays were marked with a red dot by the radiographer otherwise they were left unmarked. All the radiographers had received in-house training in interpreting x-rays.

Each x-ray was then interpreted by one of the ED junior doctors (each with similar training of at least 1-year experience post-qualification). All x-rays were then verified by a radiologist and this was the reference standard.

The data collected included the date, patient’s age, x-ray type (eg, scaphoid), radiographer’s triage result, junior doctor’s diagnosis and reference diagnosis. The x-rays were classified by the part of the body irradiated (x-ray type), such as chest x-rays.

Features considered abnormal on an x-ray depended on the x-ray type and included fractures (skeletal x-rays), cardiomegaly (chest x-rays) and dilated bowel (abdominal x-rays), thus covering a range of target disorders and are detailed elsewhere. In the high-probability (red dot) x-rays, the prevalence of abnormal findings was 77% compared with 13% in the ‘low-probability’ x-rays. Although the junior doctors were aware that a red dot indicated a higher probability of an abnormality, they were not aware of how high this probability was.

Statistical analysis

Two by two tables were derived for each of the high- and low-prevalence subpopulations. The sensitivity, specificity, likelihood ratios and diagnostic odds ratios (DOR) were used for comparison and a receiver operator characteristic (ROC) curve was constructed. While performance statistics, such as the sensitivity and specificity, could be calculated from pooling the data across all the junior doctors, this does not take into account variation in the performances between junior doctors. Furthermore, it does not allow for the effects of the x-ray type on the performances of individual junior doctors.

Hence, a hierarchical logistic regression model was constructed to study the effects of different covariates on the dependent variables, logit sensitivity and logit specificity. Junior doctors were included in the model as a random effect, and covariates on prevalence, x-ray types and broader groupings of x-ray types were also included.

As any effects of prevalence on performance may be explained by differences in performance across different x-ray types, the interaction between the prevalence and x-ray type was evaluated. Cross-level interactions between explanatory variables were also investigated by allowing the slope to vary across individual doctors. Models were compared using the log likelihood ratio test statistic (LRT), which has an asymptotic $\chi^2$ distribution with degrees of freedom (df). All analyses were completed using the statistical software R, and statistical significance was set at $p < 0.05$. A full description of the model may be found in the online appendix.
The type of x-ray a patient receives is, in part, indicative of their morbidity. Thus, the distributions of x-ray types were inspected to give some indication on whether the mix of patients (or patient-mix) varied between the high- and low-prevalence populations. If some x-ray types are more difficult to interpret than others (such as abdominal x-rays compared with tibial x-rays), then differences in the relative proportions of these may explain differences in the performance characteristics.

**RESULTS**

There were 1053 x-rays interpreted by 26 ED junior doctors following triage by a radiographer. Eighty-six were excluded due to incomplete information on the radiographers’ triage result (28), junior doctors’ diagnosis (10) and reference diagnosis (48). The remaining 967 x-rays are analysed in **table 1**.

The striking feature of these results is the change in sensitivity, specificity and positive likelihood ratio between the low- and high-prevalence populations (**table 2**). The differences are statistically significant and provide evidence against the null hypothesis that the performance characteristics of junior doctors at interpreting x-rays do not vary with prevalence.

In contrast, the DOR for each of the high- and low-prevalence populations were not statistically significantly different, being very close to each other at 37.3 (95% CI 3.6 to 101.3) and 36.1 (95% CI 21.0 to 62.3), respectively. This is consistent with the null hypothesis that the DOR is constant, which has a bearing on the shape of the ROC curve. A common DOR generates a symmetrical ROC curve, and observing how closely the points are to the curve, this informs a possible cause to the variation in the sensitivity and the specificity, namely a change in the implicit threshold for test positives as applied by the junior doctors (**figure 1**).

The x-ray distributions for each of the normal and abnormal populations are shown in **figures 2 and 3**. On inspection, the distributions are broadly similar for the high- and low-prevalence populations in each case, with only chest x-rays being an outlier in **figure 3**. This would suggest that any differences in performance between the high- and low-prevalence populations are unlikely to be due to differences in the relative proportions of x-ray type.

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**Table 1** Contingency tables showing the summary totals in each of the cells after pooling all the junior doctors

| Doctor’s diagnosis | High-prevalence population (77%) | Low-prevalence population (13%) |
|--------------------|----------------------------------|---------------------------------|
|                    | Reference standard | Reference standard | |
|                    | Positive | Negative | Positive | Negative | |
| Positive | 159  | 22      | 181     | 72       | 50   | 122   |
| Negative | 10   | 28      | 38      | 24       | 602  | 626   |
| Totals  | 169  | 50      | 219     | 96       | 652  | 748   |

Note x-rays in the high/low-prevalence population were those interpreted by the radiographer as having a high/low probability of an abnormal feature. The true prevalence is determined by the reference standard.

**Table 2** Summary performance estimates given for the independent significant covariate, prevalence. Also given are the estimates of sensitivity for each level of the covariate x-ray group, which was significant for the dependent variable logit (sensitivity)

| Model estimates of performance characteristics in significant covariates | High prevalence | Low prevalence |
|------------------------------------------------------------------------|-----------------|----------------|
| Sensitivity (%)                                                        |                 |                |
| Soft tissue x-rays                                                     | 93.7 (79.5 to 98.3) | 68.3 (44.3 to 85.3) |
| Appendicular x-rays                                                    | 97.3 (93.3 to 99.0) | 84.0 (70.3 to 92.2) |
| Axial skeletal x-rays                                                  | 58.6 (17.3 to 90.5) | 17.0 (2.4 to 63.1) |
| Summary                                                               | 95.8 (91.1 to 98.1) | 78.3 (65.7 to 87.2) |
| Specificity (%)                                                        |                 |                |
| Summary                                                               | 56.0 (41.9 to 69.2) | 92.3 (90.0 to 94.2) |
| Positive likelihood ratio                                             | 2.2 (1.6 to 3.0) | 10.2 (7.6 to 13.8) |
| Negative likelihood ratio                                             | 0.07 (0.03 to 0.17) | 0.23 (0.14 to 0.38) |
| Diagnostic Odds ratio                                                 | 37.3 (3.6 to 101.3) | 36.1 (21.0 to 62.3) |

All estimates are derived from the hierarchical regression model and take into account variation in performance between individual doctors and different x-ray groups. The covariate x-ray group has three levels: soft tissue (chest and abdominal x-rays), appendicular (limbs, hands and feet) and axial (skull, spine and sacrum). Interaction terms were not significant. 95% CIs are shown in brackets.
The effect of prevalence on the sensitivity and specificity of a diagnostic test

Figure 1  Symmetrical receiver operator characteristic curve (weighted mean diagnostic odds ratios (DOR)) for the average junior doctor. Weighted mean DOR (36.4) was derived from weighting model estimates of DORs for high-prevalence population (37.3) and low-prevalence population (36.1). Point estimates of sensitivity and 1–specificity for both populations are also given.

The effects that the change in x-ray distributions may have on performance between the two subpopulations was modelled using hierarchical logistic regression. Unsurprisingly, prevalence was a significant covariate for each of the dependent variables logit sensitivity (LRT=20.6, df=1, p~10⁻⁵) and logit specificity (LRT=42.8, df=1, p~10⁻¹¹).

In contrast, x-ray type was not a significant covariate for either logit sensitivity (LRT=34.4, df=24, p=0.078) or logit specificity (LRT=23.3, df=33, p=0.89). Owing to the number of levels to the factor x-ray type (34), this could be due to insufficient data. Therefore, x-ray types were grouped into three broad mutually exclusive groups: skeletal x-rays that were subdivided anatomically into appendicular (limbs, hands and feet) and axial (skull, facial and spine)²⁰ and soft tissue x-rays (chest and abdomen). The x-ray group was a significant independent covariate for logit sensitivity (LRT=10.88, df=2, p=0.0043) but not for logit specificity (LRT=2.74, df=2, p=0.26) (table 2). However, interaction terms between prevalence and x-ray group and across levels between x-ray groups and junior doctors were not significant for either dependent variable.

As chest x-rays were a potential outlier (figure 3), a sensitivity analysis was performed to investigate the effects of this category on the statistical significance of covariates, by including and excluding this category from the model. No significant effects were found.

**DISCUSSION**

This study demonstrated statistically significant differences in the sensitivities, specificities and positive likelihood ratios between the high- and low-prevalence populations (table 2), providing evidence that the diagnostic performance of junior doctors in interpreting x-rays does vary with prevalence. There was evidence that the sensitivity depended on the x-rays being interpreted, and although such dependence could not be demonstrated for individual x-ray types (due to sample size), it was demonstrated for broader categories of x-rays. Since the x-ray type is an indicator of the type of target disorder and therefore patient, this implies that the diagnostic performance does depend to some degree on both the type of x-ray being interpreted and the target disorder being sought.

However, this was an independent effect: analysis of the interaction between prevalence and x-ray group was not significant. The effect of the junior doctors’ performance varying with prevalence occurred irrespective of the type of x-ray being interpreted or target disorder being sought. Although performance was evaluated over different types of x-rays and multiple target disorders, these findings suggest the potential of observing such...
The question that is raised by this example is whether the effects observed may be generalised to other diagnostic tests? An example where these may occur is in the dynamic process of taking a clinical history or examining a patient, where information from previous tests such as the response to a particular question is available to inform future tests. During this process, the clinician may adjust their threshold for a positive result on the basis of the previous test results. The strength of expectation generated by the previous test results is likely to play a role in how far the clinician adjusts this threshold. Thus, a sequence of four positive responses to directed questions in a history might influence a clinician to lower their threshold for the next question, thereby increasing the sensitivity and decreasing the specificity, compared with if the four previous responses had been negative.

In this study, the test was evaluated in two separate subpopulations in which the main difference was the prevalence of abnormality. This has obvious advantages over two separate studies by controlling for a number of factors that may affect the test performance: the same junior doctors, same radiographers, same reference standard and similar patient-mixes.

Nonetheless, there are two principal limitations relating to the quality of the reference standard (a single radiologist’s opinion) and a lack of blinding between the test and the reference standard, raising the potential for review bias. It is difficult to gauge the effect a lower quality reference standard would have on performance estimates, but it is unlikely to have a differential bias between the high- and low-prevalence populations. Equally, the effects of review bias are likely to inflate estimates of the sensitivity and specificity in both the high- and low-prevalence populations and given it is differences between these performance statistics that are important to demonstrate the principle, inflated estimates in both subpopulations are less of a problem.
The effect of prevalence on the sensitivity and specificity of a diagnostic test

In the regression model, the sensitivity and specificity were treated as independent variables. A bivariate random effects model would maintain the association between the sensitivity and specificity, and individual patient data models have been suggested. While such advanced approaches may augment the analysis, they would not change the broad findings demonstrated here.

In summary, the diagnostic performance of junior doctors in interpreting x-rays does vary with pre-test probability and this seems to be predominantly based on changing the implicit threshold in response to previous test results. Furthermore, it is unlikely that these findings are confined to the example analysed here. As such, it is an area deserving of further research to establish the extent by which it affects those tests in which there is a subjective element in the execution of the test.

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