TW Hya: an old protoplanetary disc revived by its planet

Sergei Nayakshin,1,1 Takashi Tsukagoshi,2 Cassandra Hall,1 Alonna Vazan,3,4 Ravit Helled,4 Jack Humphries,1 Farzana Meru,5,6 Patrick Neunteufel,1,7 and Olja Panic8

1 School of Physics and Astronomy, University of Leicester, University Road, LE1 7RH Leicester, UK
2 Division of Radio Astronomy, National Astronomical Observatory of Japan, Osawa 2-21-1, Mitaka, Tokyo 181-8588, Japan
3 Racah Institute of Physics, The Hebrew University, Jerusalem 91904, Israel
4 Institute for Computational Science, Center for Theoretical Astrophysics and Cosmology University of Zurich, CH-8057 Zurich, Switzerland
5 Department of Physics, University of Warwick, Gibbet Hill Road, Coventry CV4 7AL, UK
6 Centre for Exoplanets and Habitability, University of Warwick, Gibbet Hill Road, Coventry CV4 7AL, UK
7 Max-Planck-Institut für Astrophysik, Karl-Schwarzschild-Str. 1, D-85748 Garching, Germany
8 School of Physics and Astronomy, University of Leeds, Leeds LS2 9JT, UK

Accepted 2020 April 17. Received 2020 April 10; in original form 2020 March 13

ABSTRACT

Dark rings with bright rims are the indirect signposts of planets embedded in protoplanetary discs. In a recent first, an azimuthally elongated AU-scale blob, possibly a planet, was resolved with ALMA in TW Hya. The blob is at the edge of a cliff-like rollover in the dust disc rather than inside a dark ring. Here we build time-dependent models of TW Hya disc. We find that the classical paradigm cannot account for the morphology of the disc and the blob. We propose that ALMA-discovered blob hides a Neptune mass planet losing gas and dust. We show that radial drift of mm-sized dust particles naturally explains why the blob is located on the edge of the dust disc. Dust particles leaving the planet perform a characteristic U-turn relative to it, producing an azimuthally elongated blob-like emission feature. This scenario also explains why a 10 Myr old disc is so bright in dust continuum. Two scenarios for the dust-losing planet are presented. In the first, a dusty pre-runaway gas envelope of a ∼40 M⊕ Core Accretion planet is disrupted, e.g. as a result of a catastrophic encounter. In the second, a massive dusty pre-collapse gas giant planet formed by Gravitational Instability is disrupted by the energy released in its massive core. Future modelling may discriminate between these scenarios and allow us to study planet formation in an entirely new way – by analysing the flows of dust and gas recently belonging to planets, informing us about the structure of pre-disruption planetary envelopes.

Key words: planets and satellites: formation – protoplanetary discs.

1 INTRODUCTION

Recent advent in the high-resolution imaging of protoplanetary discs via scattering light techniques and mm-continuum with ALMA yielded many exciting examples of sub-structures in the discs, such as large-scale asymmetries (Casassus et al. 2013), spirals (Benisty et al. 2017), dark and bright rings and/or gaps (ALMA Partnership et al. 2015; Andrews et al. 2018; Dullemond et al. 2018; Long et al. 2018), clumps and young planets (Mesa et al. 2019). In fact it is believed that most protoplanetary discs have substructures; those that do not may simply be those that have not yet been imaged at high enough resolution (Garufi et al. 2018). The fact that these substructures are seen in very young discs, and that the masses of these discs appear to be insufficient to form planetary systems that we observe (Greaves & Rice 2010; Manara, Morbidelli & Guillot 2018; Williams et al. 2019), indicates that planets form very rapidly, possibly faster than 1 Myr.

On the one hand, these observations bring new challenges. The presence of mm-sized dust in a few Myr old discs is surprising because of the rapid inward radial drift of the grains (Weidenschilling 1977; Birnstiel, Klahr & Ercolano 2012). While the radial drift can be slowed down by invoking very massive gas discs, $M_{\text{gas}} \lesssim (0.1 - 0.2)M_\odot$ (e.g. Powell, Murray-Clay & Schlichting 2017; Powell et al. 2019), other arguments point against that. Veronesi et al. (2019) shows that the prevalence of annular rather than spiral features in many of the observed discs indicates that the mm-sized particles have rather large Stokes numbers, limiting disc

* E-mail: sergei.nayakshin@astro.le.ac.uk

© 2020 The Author(s)
Published by Oxford University Press on behalf of the Royal Astronomical Society
masses to only \( \sim 1M_\odot \). Furthermore, hydrodynamical simulations and population synthesis show that planets with properties deduced from these observations should both grow in mass and migrate inwards very rapidly (Clarke et al. 2018; Lodato et al. 2019; Mentiplay, Price & Pinte 2019; Nayakshin, Dipierro & Szulagyi 2019; Ndugu, Bitsch & Jurua 2019). This would make the detection of these planets statistically very unlikely; this paradox is resolved if the disc masses are \( \sim 1M_\odot \) so that planets do not migrate rapidly (Nayakshin 2020).

Here we focus on the protoplanetary disc in TW Hydra (Kastner et al. 1997). At the distance of about 60 pc, this protostar is the closest one with a protoplanetary disc, and is probably the best studied. Despite its advanced age of \( t_\ast \approx 10 \) Myr (Weinberger, Anglada-Escudé & Boss 2013), TW Hydra continues to accrete gas at a respectable rate (\( \sim \sim 2 \times 10^{-9}M_\odot \) yr\(^{-1}\)). Its disc is the prototype for discs with cavities possibly carved by growing planets, with early observations indicating gaps on the sub-AU to a few AU scales (Calvet et al. 2002; Eisner, Chiang & Hillenbrand 2006). Recent high-resolution ALMA observations found several axisymmetric gaps in the continuum sub-mm dust emission of TW Hya, one on the scale of \( \sim 1\) AU, and two more at \( \sim 24 \) and 41 AU (Andrews et al. 2016; Huang, Wu & Triaud 2016; Tsukagoshi et al. 2016; Huang et al. 2018).

However, the currently unique feature of TW Hydra is the first ever image of a potential planet in the ALMA 1.3 mm dust continuum emission (Tsukagoshi et al. 2019; T19 hereafter). The few AU-scale emission excess is significant (12\( \sigma \) over the disc background intensity) and has an azimuthally elongated shape. T19 associated it with a circumplanetary disc of a growing Neptune mass planet. Most curiously the putative planet is located not inside the previously discovered gaps but at 51.5 AU from the star, right on the edge of a well-known cliff-like rollover in the dust disc (Andrews et al. 2012, 2016; Hogerheijde et al. 2016). In contrast, emission of many molecular tracers and from microscopic dust have broad peaks at 50–60 AU, and extending to distances as large as 100–250 AU (Kastner et al. 2015; Bergin et al. 2016; Teague et al. 2018).

Below we model the time evolution of the gas and dust components of TW Hydra’s disc and compare the resulting dust continuum emission with ALMA bands 7 and 6 (820 \( \mu \)m and 1.3 mm, respectively) and EVLA 9 mm observations of the source. We investigate several possible scenarios to try and explain both the disc morphology, with its sharp rollover of the dust disc, and the image of a putative planet positioned at the edge of that rollover. We find multiple lines of argument that challenge the standard quasi-steady-state scenario for this disc. We propose that this disc has been recently re-invigorated by mass injection from a disrupted planet.

The paper is structured as follows. In Section 2 we summarize the observations of TW Hydra relevant to this paper. In Section 3 we give simple analytical arguments that challenge the quasi-steady-state scenario. In Section 4 we present our numerical methods. In Section 5 we apply these to the quasi-steady-state disc scenario, finding significant and additional to Section 3 problems with it. We test a phenomenological Dust Source model in Section 6, in which a low-mass object on a fixed circular orbit ejects dust into the surrounding, initially dust-free, disc. This scenario proves promising but is not physically self-consistent. In Section 7 we propose that a collision between a \( \sim (30 - 40)M_\odot \) pre-collapse Core Accretion planet with a dust-rich envelope and another massive core could unbind the envelope and make the planet a dust source. In Section 8 we show that a gas giant planet formed in the Gravitational Instability scenario could be disrupted from within by its massive luminous core provided that the planet is very metal rich (\( Z \sim 0.1 \)) and its mass is \( M_p \lesssim 2M_\odot \).

Since the planet is formed in this scenario very early on (presumably at \( t \lesssim 0.1 \) Myr), survival of the planet on a very wide orbit by \( t \sim 10 \) Myr requires that TW Hydra had neither gas nor dust disc before the disruption of the planet. In Section 9 we tackle the issue of the ‘blob’ morphology in the Tsukagoshi et al. (2019) ALMA image, e.g. its spatial extent and its elongation along the azimuthal direction. We conclude with an extended discussion in Section 10.

### 2 Dusty Puzzles of TW Hydra

TW Hydra is an oddity in many regards. The mass of the mm-sized dust in TW Hya is surprisingly large, estimated at \( \sim 80M_\odot \) (after correcting to the new GAIA distance; Andrews et al. 2016). Williams et al. (2019) shows that the mean dust mass of class I sources (generally thought to be much younger than 1 Myr) is \( \sim 4M_\odot \) whereas the mean mass of class II sources is \( \sim 0.8M_\odot \), thus, despite being older by a factor of a few than an average type II disc, TW Hya’s dust disc is \( \sim 100 \) times more massive in dust than the mean.\(^1\)

The mass of \( H_2 \) gas disc in TW Hya is suspected to be very high, although there are significant uncertainties. Bergin et al. (2016) inferred TW Hya \( H_2 \) disc mass from HD line observations to be \( \gtrsim 0.05M_\odot \), but this value was revised to between 0.006 and 0.009 \( M_\odot \) by Trapman et al. (2017) with an alternative model and more data. However, as shown by Jones, Pringle & Alexander (2012), for a disc evolving viscously, its mass at age \( t_\ast \) is given by \( \dot{M}_d \approx \xi_d \dot{M}_\ast t_\ast \) where \( \xi_d \gtrsim \) a few. Here the accretion rate inferred for TW Hya is \( \dot{M}_d \approx 1.8 \times 10^{-5}M_\odot \) yr\(^{-1}\) (Ingleby et al. 2013). Independently of this argument, Powell et al. (2019) use the dust radial drift constraints to estimate the gas disc mass in TW Hya as \( \gtrsim 0.11M_\odot \).\(^2\) Such a high mass is \( \sim 2 \) orders of magnitude higher than the median gas disc mass for type II discs (Manara et al. 2018).

Fig. 1 shows the summary of TW Hydra observations that are relevant to this paper. The top left-hand panel shows the image of the source in the 1.3 mm continuum presented in Tsukagoshi et al. (2019). The two annular gaps are well known from the previous ALMA observations (Andrews et al. 2016; Tsukagoshi et al. 2016; Huang et al. 2018). The white box in the left-hand panel of Fig. 1 is centred on the location of the excess. The half widths of the excess are \( \sim 0.5 \) AU in the radial and \( \sim 2.2 \) AU in the azimuthal directions.

The bottom panel of Fig. 1 shows with the green and red curves the ALMA azimuthally averaged dust continuum intensity profiles at 1.3 mm and 820 \( \mu \)m, respectively, and the EVLA 9 mm intensity of the blue curve.\(^3\) The radial profiles of the ALMA images were extracted by averaging the full azimuthal angle except for the position angles of the millimetre blob (P.A. \( = 222^\circ - 236^\circ \) and \( 238^\circ - 252^\circ \)). For the profile of the EVLA data, we took an average over the full azimuthal angle. The profiles were made after the image deprojection under the assumption that the disc inclination

\(^1\)We shall see later that TW Hydra’s dust mass may be as small as \( \sim 15M_\odot \) if DIANA (Woitke et al. 2016) opacities (Section 4.4) are used. Williams et al. (2019) 1.3 mm opacity is quite similar to that used by Andrews et al. (2016). The higher DIANA opacities would reduce the dust mass estimates made by Williams et al. (2019) by about the same factor, maintaining the surprising mass superiority of TW Hydra’s dust disc.

\(^2\)In fact the authors assumed the age of 5 Myr. For a 10 Myr source the required disc mass to delay the dust drift sufficiently would be \( \lesssim 0.2M_\odot \).

\(^3\)The data are downloaded from Disks at EVLA program: https://safe.nrao.edu/evla/disks/.
is 7° and the position angle is −30° from the North. We see that the ALMA continuum emission plunges by an order of magnitude from $R \approx 52$ AU to $R = 70$ AU. This behaviour is not apparent in the EVLA data, but because the beam size is ~15 AU it is possible that the intrinsic disc $I_e$ also has a similarly sharp rollover at the same location.

While dust discs much smaller than the gas discs as traced by CO emission are not uncommon, and while there are other dust discs with sharp outer cutoffs (e.g. Trapman et al. 2019), TW Hya is certainly the best resolved disc of this kind. Hogerheijde et al. (2016) searched for a broken power-law fit to ALMA data at the wavelength of 820 μm. They found the power-law index of $p \approx$
−0.5 before the break, and $\Sigma_{\text{dust}} \propto R^{-3}$ beyond the break. We show this $\Sigma_{\text{dust}}(R)$ profile with the dot-dash-violet curve in Fig. 1. Note that the location of the T19 planet coincides very well with the break in dust $I_\lambda$ and $\Sigma_{\text{dust}}$. The gas surface density profile is much harder to constrain although it is clear that the gas disc extends at least to 200 AU. The three black curves in the bottom panel of Fig. 1 show three gas surface density models from the literature. While the total gas disc mass varies by about an order of magnitude between these, it is clear that the gas distribution is not as compact as that of the dust.

3 ANALYTICAL PRELIMINARIES: THE STEADY-STATE SCENARIO

In the classical protoplanetary disc paradigm, the discs are formed during the collapse of the parent molecular cloud and persist until dispersed after $\sim (3–10)$ Myr (Alexander et al. 2014). This steady state scenario is explored numerically in Section 5, here we scrutinize it with more transparent analytical arguments.

3.1 Disc model

The accretion rate on to the star in the viscous steady state is (Shakura & Sunyaev 1973)

$$M_* = 3\pi \nu \Sigma = 3\pi \alpha \left(\frac{H}{R}\right)^2 \frac{v_\text{K}}{\eta} \nu R \Sigma,$$

where $v_\text{K} = \Omega_\nu R = (GM_*/R)^{1/2}$ is the local circular Keplerian speed, $\Sigma$ is the local gas surface density, $\nu = \alpha c_s R$ is the disc viscosity, $\alpha$ is the viscosity parameter, $H$ is the disc vertical scale height, and $c_s$ is the gas sound speed. We assume that the disc mid-plane temperature is given by

$$T = T_0 \left(\frac{R_0}{R}\right)^{1/2},$$

where $T_0 = 18$ K is the gas temperature at the planet location, $R_0 = 51.5$ AU (this temperature profile is very similar to the mid-plane temperature profile derived in Huang et al. 2016). For reference, $v_\text{K} = 3.7$ km s$^{-1}$, $c_s = 0.25$ km s$^{-1}$, and $H/R \approx 0.07$ at $R = R_0$. In the whole of Section 3 we also assume that

$$\Sigma(R) = \Sigma_0 \frac{R_0}{R}. $$

Equation (1) constrains the product of $\alpha \Sigma_0$. We shall use additional considerations to constrain $\Sigma$, which then limits $\alpha$ via equation (1).

3.2 Gas accretion constraints on the disc mass

Numerical integrations of viscously evolving discs show that the accretion rate on to the star is large at early times and then decreases (Jones et al. 2012). The product of the accretion rate and current time $t$ remains approximately constant initially and later also decreases (because $M_*$ drops with time). Usefully for us here, the disc mass at age $t_*$ is given by

$$M_* \approx \xi_d M_* t_* \approx 0.1 M_\odot \left(\frac{\xi_d}{3}\right),$$

where $\xi_d \sim 1$ is a dimensionless number (Jones et al. 2012), and we used $M_* = 1.8 \times 10^{-9} M_\odot$ yr$^{-1}$ and $t_* = 10$ Myr.

3.3 Dust drift constraints

As previous authors (Andrews et al. 2012) we find that particles of size $a \gtrsim 1$ mm are required to explain ALMA observations. The radial dust drift velocity is (Whipple 1972)

$$v_\text{dr} = \frac{\eta}{\Sigma} \left(\frac{H}{R}\right)^2 \frac{v_\text{K}}{\eta} \nu R \Sigma,$$

where $\eta = 1.25$ given our model disc pressure profile, and the Stokes number is given by

$$St = \frac{\pi \rho_a a}{\nu R} \Sigma,$$

with $\rho_a = 2.1$ g cm$^{-3}$ (Woitke et al. 2019) being the grain material density. For a $p = 3.5$ power-law grain size distribution with maximum grain size $a$, the appropriate grain size to use in equations (5) and (6) in the small $St \ll 1$ regime is the mean grain size, $a_{\text{mean}} = a/3$ (see Section 4.3). Demanding the dust particle drift time-scale to be 10 Myr at the location of T19 planet we arrive at the minimum gas surface density at $\sim 50$ AU of

$$\Sigma_0 > 100 \text{ g cm}^{-2} \frac{1 \text{ mm}}{a}. $$

With the observed gas accretion rate of $\dot{M}_* \approx 1.8 \times 10^{-9} M_\odot$ yr$^{-1}$, we simultaneously have that

$$\alpha < 10^{-4}. $$

The disc mass enclosed within radius $R$ is then

$$M_{\text{disc}}(R) = 2\pi R \Sigma_0 \frac{R}{R_0},$$

This is larger than $M_0 = 0.11 M_\odot$ found by Powell et al. (2019), mainly because they assumed that TW Hydra is younger (5 Myr).

The mass in equation (9) is uncomfortably large for many reasons. First, the typical gas mass of a few Myr old disc is estimated at $\sim 10^{-3} M_\odot$ (Manara et al. 2018). Secondly, such a massive disc should be strongly self-gravitating since the Toomre (1964) parameter is

$$Q = \frac{c_s \Omega}{\pi G \Sigma} \sim 0.6 $$

when evaluated at $R = R_0$. We expect the disc to show spiral density structure, and in fact be fragmenting for such a low $Q$. Indeed, a 3D Phantom SPH calculation confirmed that the disc with the structure introduced at Section 3.1 and extending to 200 AU (as observed) fragments due to self-gravity.

Another interesting inference from the dust drift constraints is the dust-to-gas ratio in the TW Hydra disc. According to Hogerheijde et al. (2016), $\Sigma_{\text{dust}} \approx 0.2$ at $R \sim 50$ AU (although this depends on the dust opacity and size distribution). Hence, $\xi_0 = \Sigma_{\text{dust}}/\Sigma \approx 0.003$. This is only slightly larger than that derived by Woitke et al. (2019) for TW Hydra, who obtained $\xi_0 \approx 0.002$. If the observed emission of the T19 feature is due to a circumplanetary disc around the planet, we would then expect the disc to have a dust-to-gas ratio smaller than $\xi_0$ because dust in the circumplanetary disc is expected to drift into the planet faster than the gas component of the disc does (similar to the protoplanetary disc case). Therefore, we conclude that the minimum gas mass of the circumplanetary disc (CPD) is

$$M_{\text{cpd}} > M_{\text{cpd-dust}} \xi_0^{-1} \approx 10 M_0, $$

where $M_{\text{cpd-dust}} \approx 0.03 M_0$ is the dust mass of the T19 feature (Tsukagoshi et al. 2019). This CPD mass is surprisingly high and would require the planet itself to be much more massive, e.g.
many tens of $M_\odot$ to maintain dynamical stability. This high $M_p$ in combination with high $M_\odot$ is ruled out due to planet migration (Section 3.6) and spectral constraints (Section 5).

### 3.4 Dust particles maximum size

Here we discuss three processes that limit grain growth in our numerical models below. We also use these results to argue that the quasi-steady-state scenario cannot naturally explain the relatively small grain size in this old disc (cf. further Section 10.1, item (vi)).

Birnstiel et al. (2012) conclude that dust particle collisions due to radial drift are not likely to be a dominant mechanism of dust size regulation. For the steady state scenario of TW Hydra disc in particular, the drift velocity can be estimated by requiring the dust to not drift all the way into the star in 10 Myr:

$$v_{dr} \lesssim \frac{R_0}{10 \text{ Myr}} \approx 0.025 \text{ m s}^{-1}.$$  \tag{12}

Grains of similar sizes collide at $\sim 1/2$ of this velocity, e.g. at just about 1 cm s$^{-1}$. This velocity is two orders of magnitude smaller than the grain breaking velocities inferred from experiments and typically considered in the field, $v_{br} \sim 10$ m s$^{-1}$. Note however that this process can be dominant for planet-disruption scenarios where the relevant time-scale is $\sim 10^5$ yr.

The grain growth time is finite. Birnstiel et al. (2012) introduce the ‘drift limit’ to the maximum grain size as the grain size to which the grains grow before they are efficiently removed by the radial drift:

$$a_{\text{drift}} = 0.55 \frac{2}{\pi} \frac{\Sigma_{\text{dust}}}{\eta \rho_a} \left( \frac{R}{H} \right)^2 = 54 \text{ mm}$$  \tag{13}

at the location of the T19 planet (we used here $\Sigma_{\text{dust}} = 0.2$ g cm$^{-2}$ from Hogerheijde et al. 2016). This value is quite large, indicating that this process is also unlikely to stem grain growth in TW Hydra.

Finally, gas turbulence also sets a maximum grain size (Weidenschilling 1984), which in the limit of small Stokes number yields

$$a_{\text{turb}} = \frac{f_1}{3\pi} \frac{\Sigma}{\rho_a \alpha_t \Sigma_0} v_{br}^2.$$  \tag{14}

Here we used the turbulent viscosity parameter $\alpha_t$, which may in general be different from the Shakura & Sunyaev (1973) $\alpha$ viscosity parameter introduced previously. The latter parameterizes the efficiency of the angular momentum transfer and subsumes in itself both gas turbulence and the effects of possible large-scale magnetic torques (Bai & Stone 2013; Bai 2016). Since $\alpha \geq \alpha_t$, we estimate the minimum size set by turbulence via setting $\alpha_t = \alpha$:

$$a_{\text{turb}} \gtrsim 6 \text{ mm} \left( \frac{v_{br}}{1 \text{ m s}^{-1}} \right)^2 \frac{\Sigma_0}{100 \text{ g cm}^{-2}}.$$  \tag{15}

where $\alpha_t = 10^4 \alpha$ (cf. equation 8). For the typical values of $v_{br} \sim 10$ m s$^{-1}$ employed in the literature (e.g. Birnstiel et al. 2012), grains grow much larger than $\sim 1$ mm and then drift inward too rapidly (cf. Section 3.3). Since the observed gas accretion rate on TW Hydra sets the constraint $\alpha \Sigma_0 = \text{const}$ (cf. Section 3.1), we see that the scaling in equation (14) is

$$a_{\text{turb}} \propto v_{br}^2 \Sigma_0^2.$$  \tag{16}

This shows that a less massive disc would naturally result in more reasonable maximum grain sizes, avoiding the unwelcome necessity to demand that $v_{br}$ is as small as $\sim 0.2$ m s$^{-1}$.

### 3.5 The sharp dust rollover in TW Hydra

TW Hydra displays a cliff-like rollover in the dust density distribution at separation $R \approx 52$ AU (Andrews et al. 2012; Hogerheijde et al. 2016; Tsukagoshi et al. 2019). The observed rollover can be fit with a power-law $\Sigma_{\text{dust}} \propto R^{-8}$ at $R \gtrsim 50$ AU (Hogerheijde et al. 2016). In the context of the standard paradigm for protoplanetary discs, the separation of the dust and the gas may be expected due to the radial drift of the dust and the viscous spreading of the gas disc (e.g. Powell et al. 2019; Rosotti et al. 2019; Trapman et al. 2019).

Let us consider the dust radial drift time-scale dependence on distance $R$:

$$t_{\text{dr}} = \frac{R}{v_{dr}} \propto \frac{R \Sigma}{a(R)},$$  \tag{17}

where $a(R)$ is the radius-dependent grain size, and we assumed the low Stokes number limit. Steady-state discs usually have $\Sigma R$ $\approx \text{const}$, as we also assumed in equation (3). Thus a decreasing grain size with increasing $R$ means that $t_{\text{dr}}$ increases with $R$.

This in turn implies that dust density gradients are eroded over time. Consider two radii in the disc, $R_1 < R_2$, and $\Sigma_1 > \Sigma_2$. Since the drift time-scale at $R_1$ is shorter than that at $R_2$, the dust surface density at $R_1$ drops with time faster than it does at $R_2$, and hence the ratio $\Sigma_1/\Sigma_2$ decreases with time.

Therefore, if the TW Hydra dust distribution does evolve from some initial distribution, then that distribution must have had an even steeper rollover than the currently observed $\propto R^{-8}$ one. It seems rather contrived to demand such a sharp initial dust edge at time $t \approx 0$.

### 3.6 Planet migration constraints

The type I migration time-scale of T19 planet is very short:

$$t_{\text{mig1}} = \frac{1}{2 \gamma \Omega} \frac{M_p^2}{M_\odot} \left( \frac{H}{R} \right)^2 \approx 4 \times 10^4 \text{ yr} \frac{100 \text{ g cm}^{-2}}{\Sigma_0} \frac{10 \text{ M}_\odot}{M_p},$$  \tag{18}

where the dimensionless factor $\gamma$ (Paardekooper et al. 2010) evaluates to $\gamma = 2.5$ in our disc model. The planet migration time is less than 1 per cent of TW Hydra’s age. Assuming that we are not observing the system at a special time, TW Hydra should hatch $\sim 100$ such planets over the course of its protoplanetary disc lifetime for us to have a decent statistical chance to observe it. This does not appear reasonable; most likely the gas disc is much less massive.

### 4 METHODOLOGY

We model the time-dependent evolution of dust and gas components in a 1D azimuthally averaged viscous disc with an embedded planet that can optionally lose a part of its mass to the disc.

#### 4.1 Gas and planetary dynamics

Our code builds on the work of Nayakshin & Lodato (2012), who modelled the time-dependent evolution of a viscous gaseous disc in azimuthal symmetry, with the disc interacting with an embedded planet via gravitational torque and optionally exchanging mass. Without the mass exchange, the planet modifies the disc structure near its orbit only via these torques; the reverse torques from the disc on to the planet force it to migrate, usually inward. The corresponding equations for the gas surface density $\Sigma$ are equations...
The diffusion equation for the dust is

\[ \frac{\partial \Sigma \delta \rho}{\partial t} + \frac{1}{R} \frac{\partial}{\partial R} \left( R \Sigma \delta \rho v_d \right) = \frac{1}{R} \frac{\partial}{\partial R} \left( R D \Sigma \delta \frac{\partial}{\partial R} \left( \frac{\Sigma \delta}{\Sigma_1} \right) \right), \]

where the full dust drift velocity given by the sum of the radial drift velocity (equation 5), the additional component due to the gas radial flow and the gravitational torque term from the planet (see equation 16 in DiPierro & Laibe 2017, for the full expression). \( D \) is the turbulent diffusion coefficient for dust, which is related to the turbulent gas viscosity \( \nu = \alpha_{\text{turb}} c_s H \) via

\[ D = \frac{\nu}{1 + \text{St}^2}, \]

where the Stoke number is given by equation (6).

### 4.2 Dust disc evolution

Following DiPierro & Laibe (2017) we extend the code to include dust evolution in the disc, although setting \( \epsilon = \Sigma_{\text{dust}}/\Sigma = 0 \) in their relevant equations as we assume the dust to be in the test particle regime. The time-dependent radial drift and turbulent diffusion equation for the dust is

\[ \frac{\partial \Sigma \delta \rho}{\partial t} + \frac{1}{R} \frac{\partial}{\partial R} \left( R \Sigma \delta \rho v_d \right) = \frac{1}{R} \frac{\partial}{\partial R} \left( R D \Sigma \delta \frac{\partial}{\partial R} \left( \frac{\Sigma \delta}{\Sigma_1} \right) \right). \]

### 4.3 Grain size evolution

Equation (20) is designed to follow the evolution of dust particles of a fixed size (Stokes number). It is desirable to extend the method to a distribution of grain particles. It is currently prohibitively expensive to model numerically the grain particle size evolution together with the spatial evolution of grains. A physically reasonable approximation, commonly employed in the literature, is to assume that the dust follows a power-law size distribution at all locations in the disc, \( d\Sigma/d\alpha \propto \alpha^{-p} \), with \( p = 3.5 \) for grain sizes between a minimum and a maximum, \( \alpha_{\text{min}} \leq \alpha \leq \alpha_{\text{max}} \). The maximum grain size is allowed to evolve in space and time due to grain growth and collisions (cf. Birnstiel et al. 2012; Rosotti et al. 2019; Vorobyov & Elbakyan 2019). The minimum grain size is of a little consequence at mm wavelengths (e.g. see the top left-hand panel in fig. 3 in Woitke et al. 2019) and so we fix \( \alpha_{\text{min}} = 0.05 \mu m \). Note that for \( p = 3.5 \), most of the mass is at the largest sizes of dust particles, and the mean grain size is \( \alpha_{\text{mean}} \approx \alpha/3 \). By following the dynamics of particles with size \( \alpha_{\text{mean}} \) we then follow the dynamics of the bulk of the dust (as also done, for example, by Rosotti et al. 2019).

We start the simulations with the maximum grain size being small everywhere in the disc, \( \alpha(R) = 1 \mu m \). We then allow the grains to grow until the maximum grain size reaches either one of the three well known maximum grain size constraints – the turbulent fragmentation, the radial drain, or the radial drift fragmentation limits (Birnstiel et al. 2012) – as described in Section 3.4.

### 4.4 Computing the disc emission spectrum

Once we have the dust surface density and the maximum grain size distributions for all disc radii, \( \Sigma_{\text{d}} \) and \( \alpha(R) \), we compute the dust optical depth

\[ \tau_d = \kappa(\lambda, \alpha) \Sigma_d(R), \]

where \( \kappa(\lambda, \alpha) \) is the DIANA dust opacity (Woitke et al. 2016) computed for the maximum grain size \( \alpha \) and radiation wavelength \( \lambda \). Both scattering and absorption opacities are included in \( \kappa(\lambda, \alpha) \).

We used an amorphous carbon fraction of 26 per cent, higher than the standard value used by Woitke et al. (2016). We found this to be necessary to fit the relative luminosities of TW Hydra in 820 \mu m and 1.3 mm wavelengths. We subsequently found that this is very close to the 25 per cent amorphous Carbon fraction derived by Woitke et al. (2019) for TW Hydra.

We compute the disc surface brightness at radius \( R \) as

\[ I_c(R) = \zeta \, \mathcal{B}_c \left( T(R) \right) \left( 1 - e^{-\tau_d} \right), \]

where \( T(R) \) is the local disc mid-plane temperature, and \( 0 < \zeta \leq 1 \) is the dimensionless function describing the disc emissivity reduction due to dust scattering given by equation (11) in Zhu et al. (2019). As shown by these authors, when \( \tau_d \ll 1 \), equation (23) reduces to the standard optically thin expression (used by, e.g. Andrews et al. 2016) for the radiation intensity emitted by the disc, which has no scattering contribution. However, when \( \tau_d \gg 1 \), the scattering albedo may produce a non-trivial and significant reduction of the dust emissivity from the blackbody function \( \mathcal{B}_c \); this reduction is described by the function \( \zeta \). As TW Hydra’s disc inclination to us is very small (\( i \approx 7^\circ \), \( \cos i \approx 0.99 \)), we shall for simplicity set \( i = 0 \) in this paper.

### 5 THE QUASI-STEADY STATE DISC SCENARIO

As shown in sub-section 3.2 and 3.3, the gas disc must be very massive to both feed TW Hyd and prevent the mm-sized dust drifting into the star in 10 Myr. We set the initial disc mass to 0.15 \( M_\odot \) to avoid it becoming self-gravitating. For this disc we found that the viscosity parameter of \( \alpha = 10^{-4} \) yields stellar accretion rate between (1 - 2) \times 10^{-6} \( M_\odot \) yr\(^{-1}\) at time between \( \sim 3 \) and 10 Myr, as appropriate for TW Hyd.

For simplicity, we artificially hold a planet on a fixed orbit at the location of excess emission in T19. For planets with mass \( M_p \sim 10 M_\oplus \), the planet migration time-scales are uncomfortably short for massive gas discs, \( t_{\text{mig}} \lesssim 0.1 \) Myr (see equation 18). We explored the parameter space of such more self-consistent models and found that they are challenged by the data even more than the fixed planet orbit models. For brevity we do not show their results here.
Here we present a simulation with the following parameters: an initial disc mass $M_d = 0.11 M_\odot$ (as suggested for TW Hydra by Powell et al. 2019), the initial dust-to-gas ratio of $\Sigma_{\text{dust}}/\Sigma = 0.03$, and the planet mass $M_p = 10 M_\oplus$. The disc viscosity parameter $\alpha = 1.5 \times 10^{-4}$ was constrained by demanding the gas accretion rate on to the star to be close to the observed value. The turbulent viscosity parameter $\alpha_{\text{turb}}$ was set equal to $\alpha$. Note that lower values of $\alpha_{\text{turb}}$ are unlikely based on the analysis in Dullemont et al. (2018). The maximum grain size in TW Hydra disc is at least 1 mm (Andrews et al. 2016). To achieve this, the dust breaking velocity had to be set much lower in this simulation, $v_{\text{br}} = 0.3 \text{ m s}^{-1}$, than the value usually assumed in literature ($v_{\text{br}} \sim 10 \text{ m s}^{-1}$, e.g. Drążkowska, Windmark & Dullemont 2014; Rosotti et al. 2019).

Fig. 2 shows the model disc intensity at wavelength 1.3 mm (top panel) and the dust disc surface density (bottom panel) at three different times. The observed ALMA intensity and the dust surface density profile deduced by Hogerheijde et al. (2016) for TW Hydrae are shown with the solid green curves in the top and bottom panels, respectively. This deduced $\Sigma_{\text{dust}}$ is scaled down by a factor of 3 as the DIANA opacities we use are higher by a factor of a few. The bottom panel also shows the maximum grain size $a$ at time $t = 6$ Myr.

We observe a number of features expected from the presence of a massive planet in a disc (Rice et al. 2006; Pinilla et al. 2012; Dipierro & Laibe 2017; Zhang et al. 2018). The planet acts as a dam for the dust, so that a bright outer rim appears behind it. Inside the orbit of the planet, the dust is free to drift into the star, and hence a deep and wide gap appears there. Note that the disc intensity in the top panel is not simply linearly proportional to the dust surface density from the bottom panel. This occurs because the dust grain sizes vary with location in the disc, and even more importantly because the disc intensity saturates at the Blackbody function $B_s(T)$ at very high optical depths $\tau_d$. As a specific example, consider radius $R \approx 30 \text{ AU}$ in Fig. 2. While $\Sigma_{\text{dust}}$ at this radius decreased by almost an order of magnitude going from $t = 0.45 \text{ Myr}$ to $t = 2 \text{ Myr}$, the intensity of the disc emission at that radius did not vary at all.

Overall we see that the model disc intensity is very different from the one observed, and the dust surface densities are also different from the broken power-law fit of Hogerheijde et al. (2016). Although the disc intensity and $\Sigma_{\text{dust}}$ vary with model parameters, in all of the cases we experimented with the model always contradicts the observations: for a sufficiently massive planet, the dust emission should be suppressed inside the planetary orbit and that there should be a bright rim behind it. The observations show no suppression of the dust emission at or inside the orbit of the planet, and the disc intensity does not display a bright rim behind it.

### 5.2 3 Earth mass planet at 51.5 AU

Fig. 3 shows a calculation entirely analogous to that shown in Fig. 2, except the planet mass is set at $M_p = 3 M_\oplus$. In this case the planet produces only a barely noticeable depression in dust surface density just around its orbit, as the observations demand. The results of this calculation are very similar to that with any smaller planet mass, $0 \leq M_p \leq 3 M_\oplus$.

Fig. 3 shows that, with the planet effects on the disc reduced, the model may actually yield a flat emissivity profile in the inner disc followed by a steep decline, exactly as needed to explain TW Hydra’s ALMA data. This occurs due to the already mentioned saturation of the intensity in the inner disc where it becomes optically thick. For example, the dash-dotted cyan curves ($t = 6 \text{ Myr}$) in Fig. 3 appears most promising, with the break in the disc intensity occurring right where needed. However, the saturation of disc intensity at the Blackbody function is also the reason why this scenario contradicts the data strongly.

Fig. 4 shows the disc intensity at $t = 6 \text{ Myr}$ in three wavelengths in the top panel, along with the corresponding ALMA and EVLA observations. The bottom panel shows the respective disc scattering plus absorption optical depth for these wavelengths, the dust surface density $\Sigma_{\text{dust}}$ (which is the same as the cyan line from the bottom panel in Fig. 3), and the maximum grain size $a$. While the model fits the broken power-law shape of the intensity profile of the disc in the two ALMA bands, it is too bright by a factor of $\sim 3$. This cannot be ‘fixed’ by any changes in the dust opacity model or variations in $\Sigma_{\text{dust}}$. To understand why, note the purple curve in the top panel of Fig. 4 that shows the disc intensity profile in the optically thick limit, i.e. $I_s = B_s$ everywhere. We now see that the break in the disc emissivity profile in the two ALMA bands indeed occurs where its optical depth exceeds unity somewhat (where the dust absorption only optical depth is $\sim 1$).

The only physical way to make the model disc appropriately bright in the ALMA bands is to demand that it becomes optically...
thick not at $R \sim 50$ AU but at $R \sim 30$ AU. However, that would contradict the observed intensity profile. Further, 9 mm EVLA data pose a separate but physically similar challenge. To match the correct intensity level at $\sim 50$ AU in this wavelength the disc needs to be very optically thin. This then implies that the EVLA emission must track the strong rise in $\Sigma_{\text{dust}}$ inward, but the observed profile is rather flat in the $\sim 30–60$ AU region.

In fact, it is well known that the outer disc in TW Hydra must be optically thin in sub-mm and longer wavelengths from pre-ALMA photometry (the integrated disc luminosity) data: the luminosity of the source rises as $\propto \nu^{2.6}$ rather than $\propto \nu^{2}$ as expected for the optically thick disc (e.g. see Section 3 and fig. 1 in Pascucci, Gorti & Hollenbach 2012). Furthermore, the image of the T19 excess emission is significantly smaller than the disc pressure scale height, and that too implies that the disc is optically thin in the ALMA bands (see Section 9.1).

Summarizing, the quasi-steady state scenario cannot fully account for the observed continuum dust emission from TW Hydra’s protoplanetary disc. In Section 9 and Section 10.1 we shall see that it faces many additional challenges.

6 A PHENOMENOLOGICAL DUST SOURCE MODEL

We now make a single but significant alteration to the physical setup of our simulations. We assume that the planet ejects dust in the surrounding disc. The simulation setup and initial conditions are exactly the same as those presented in Section 5.2 except that we assume a negligible amount of dust into the gaseous disc at $t = 0$ for simplicity. The dust mass-loss rate from the planet is a free parameter of the model; we found that choosing $\dot{M}_Z = 6 \times 10^{-6} M_\oplus$ yr$^{-1}$ (with other parameters of the model unchanged) provides a somewhat promising spectral model. As in Section 5.2 we keep the planet mass and orbital radius fixed for now, even though this violates both mass conservation and Newton’s second law.

The dust lost by the planet is deposited in a relatively narrow ring with a Gaussian profile around the planet location, with the surface density deposition rate given by

$$\dot{\Sigma} = C \exp \left[ -\frac{(R - R_p)^2}{2w_{\text{inj}}^2} \right], \quad (24)$$

where $R_p$ is the current position of the planet, and $w_{\text{inj}} = 0.15R_p$ is the width of the Gaussian. The normalization constant $C$ ensures that the mass injection rate into the disc is equal to the planet mass-loss rate $\dot{M}_Z$. Through numerical experimentation we found that our results are insensitive to the exact injection profile as long as it is not too broad, and while $w_{\text{inj}} \ll R_p$.

Fig. 5 shows the disc intensity at 1.3 mm (top panel), $\Sigma_{\text{dust}}$, and maximum grain size $a$ (bottom panel) at several different
times. Since initially $\Sigma_{\text{dust}}$ is very low, the dust growth time is long everywhere but accelerates as more and more dust appears in the disc around the planet location. The dust grows to the (observationally required) size of $\sim 1$ mm before grain fragmentation stems grain growth. Initially, while the dust is small, dust particles diffuse both inward and outward (e.g. see the $t=1$ Myr snapshot). However, when grains become sufficiently large, the radial drift starts to blow them inward from their injection site preferentially. Therefore, a quasi-steady state dust profile gets established. This profile (e.g. the red dotted curve in the bottom panel of Fig. 5) is qualitatively similar to the Hogerheijde et al. (2016) broken power-law $\Sigma_{\text{dust}}$ profile (the solid green curve in the bottom panel). Likewise, the resulting disc intensity of this model at $1.3$ mm reaches a steady state profile somewhat similar to the observed one.

Fig. 6 examines the disc intensity in three wavelengths (top panel) and shows the disc properties (bottom panel) at time $t=5$ Myr. Comparing the figure with Fig. 4, we note that the present model has a very sharp rollover in $I_{\nu}$ behind the planet not because of the opacity transition at that point but because the dust surface density $\Sigma_{\text{dust}}$ (black curve) nose dives at $51.5$ AU. The luminosity of this model is closer to what is observed, and can also be scaled down without a significant change in the profile (except for the innermost region where the model disc is optically thick) by a simple reduction in the free parameter $M_F$. Furthermore, there is a natural casual association between the location of the planet and the rollover behind its orbit in this scenario.

The $\lambda=9$ mm EVLA intensity of the model, on the other hand, is still problematic. Furthermore, this is a phenomenological model that contradicts physics strongly. The planet mass is kept constant at $M_p=3 M_\oplus$, whereas the dust mass actually present in the disc at $t=5$ Myr is $M_d \approx 25 M_\oplus$. Increasing the planet mass at $t=0$ to a value exceeding $M_d$ would solve the mass budget problem, but as we saw in Section 5.1, a planet with mass of $\sim 10 M_\oplus$ would produce a very deep gap in the dust disc, contradicting the observations. Further, such a massive planet would migrate inward extremely rapidly, e.g. on the time-scale of $t_{\text{mig}} \sim 10^5$ yr for the disc model used in this section, invalidating the fixed orbit assumption. As the time-scale for establishing the quasi-steady state dust distribution in this model is a few Myr (cf. the cyan curves in Fig. 6), this is a fatal flaw – the planet ends up in the star faster than this steady state is reached.

7 A DESTROYED CORE ACCRETION PLANET

7.1 Physical motivation

Motivated by the successes and failures of the model presented in Section 5.2, we now attempt to build a physically motivated model based on the core accretion scenario for planet formation (Pollack et al. 1996). Core accretion scenario planets exist in two physically very different states. After the collapse of the gas envelope around a massive solid core (Mizuno 1980; Stevenson 1982; Pollack et al. 1996).
On the other hand, before the gas accretion runaway, the planet mass is thought to be no more than $\lesssim 30 - 50 M_\oplus$, with the solids making up the majority of this mass, and the outer radius of the gas envelope $\sim$ tens of $R_1$ (e.g. see fig. 2 in Mordasini et al. 2012b). Previous models assumed that most of the solids get locked into the core, separating cleanly from the gaseous envelope. However, more recent work (Lozovsky et al. 2017; Brouwers, Vazan & Ormel 2018; Podolak, Helled & Schubert 2019) shows that most of solids are vaporized before reaching the core and are suspended as gas in the hydrogen–helium mixture. The opacity of these metal-rich gas envelopes may be significantly higher than that of the traditionally assumed Solar composition ones. Additionally, modern 3D calculations of gas and dust accretion onto cores indicate complex circulating patterns of flows which tend to recycle material from various depths in the planetary atmosphere (Ormel, Kuiper & Shi 2015a; Ormel, Shi & Kuiper 2015b; Cimerman, Kuiper & Ormel 2017; Lambrechts & Lega 2017). These flows make it harder for the grains to grow and sediment into the core.

Consider now a planet–planet collision energetic enough to actually unbind a Core accretion planet. Taking a cue from the stellar collisions theory (Benz & Hills 1987), the relative velocity of the two equal mass planets at infinity, $v_\infty$, must exceed 2.3 times the escape velocity from the surface of the planet, $v_{\text{esc}} = \sqrt{2GM/\text{R}}$. The required collision velocity to unbind two equal mass planets is hence

$$v_\infty \sim \begin{cases} 100 \text{ km s}^{-1} & \text{for } M_p = 1 M_\oplus, \\ 3 \text{ km s}^{-1} & \text{for } M_p \sim 20 M_\oplus. \end{cases} \quad (25)$$

The circular Keplerian velocity at 52 AU is less than 4 km s$^{-1}$. Collisions of CA post-collapse gas giants will lead to mergers with only a small amount of mass escaping (Benz & Hills 1987); collisions of pre-collapse planets may unbind them. It is also possible that a merger of pre-collapse planet and a massive core will lead to a common envelope like evolution, in which the cores spiral in closer together while unbinding the envelope (e.g. Ivanova et al. 2013). The aforementioned high opacity makes it all the more likely that the energy deposited by the cores in the envelopes will not escape via radiation but will drive the envelope loss.

We therefore explore a model in which a pre-collapse CA planet is a source of dust. This planet may spend a long time (a few Myr) gaining its significant mass (e.g. see Pollack et al. 1996). In a massive disc studied in Section 6, such a planet would be lost into the inner disc within a very small fraction of this time due to planet migration. The migration time-scale for planets scales as $\propto \Sigma^{-1} \propto M_p^{-1}$ (equation 18). Therefore, to make this scenario plausible we must demand the gas disc to be significantly less massive than 0.11 $M_\odot$. We pick rather arbitrarily a value of $M_d = 2 \times 10^{-4} M_\odot$ while keeping the initial shape of $\Sigma$ (equation 19) the same. The results do not depend very strongly on $M_d$. Since the gas accretion rate in the disc is $\dot{M}_p = 3 \pi \alpha \Sigma H \Sigma$, we must increase the disc viscosity coefficient $\alpha$ to ensure the gas accretion rate remains the same. We thus set $\alpha = 2 \times 10^{-2}$. The changes to the values of the disk mass and disc viscosity parameter are important for dust dynamics. A higher $\alpha$ implies that the planet gravitational influence on the disc in its vicinity is significantly reduced. More massive planets may be present in the disc without opening a deep gap that would contradict observations.

### 7.2 Numerical results

Fig. 7 and 8 shows the results for a simulation started with initial planet mass $M_p = 38 M_\oplus$. For simplicity we assumed a uniform planet composition, with metallicity $Z = 0.5$. Both gas and dust are injected into the disc at a constant (and equal because $Z = 0.5$) rate of $\dot{M}_g = 2 \times 10^{-4} M_\oplus \text{yr}^{-1}$ until the planet mass drops to 10 $M_\oplus$. The planet mass is reduced accordingly as it loses mass. To exemplify the weak dependence of our results on the exact dust injection profile, the width of the Gaussian is here set to $w_\text{ini} = 0.05 R_\text{p}$ (cf. equation (24); this is three times narrower than in Section 6). Unlike the phenomenological model of Section 6, the planet is free to migrate, but on the account of the low disc mass it migrates very little during this simulation, from the starting radius of $R = 53$ to 51.5 AU.

On the whole we see that the dust profile, and the resulting disc intensity in the three wavelengths, is quite similar to those obtained in the phenomenological massive disc model (Figs 5 and 6). As in the latter model, the disc emissivity has a very sharp – in fact too sharp compared with the observation – rollover behind the orbit of the planet. The similarity in the results despite the difference in the metallicity $Z(M)$ of the envelope is expected to increase towards the core. Here we explore the simplest constant $Z$ case to contrast it to the more realistic scenario explored in Section 8.
gas disc mass of a factor of 50 between the two models shows that there is a certain degeneracy in the model parameters, e.g. a higher value of $\alpha$ could be compensated for by a higher $v_{\text{tr}}$.

8 GI PLANET DISRUPTION

8.1 Physical motivation and constraints

In Section 7.1 we argued that a core accretion planet may lose a major fraction of its gas-dust envelope if two conditions are satisfied: (i) the envelope is in the extended, pre-collapse state; (ii) a significant energy is injected in it, e.g. via collision with another massive core. We now detail conditions under which a GI planet disruption could be relevant to TW Hydra’s observations.

8.1.1 The need for a very rapid primordial disc dissipation

In the Gravitational Instability (GI; Kuiper 1951) theory for planet formation, massive and very young gaseous discs fragment at separations $\sim 50–100$ AU on to jovian mass gas clumps (e.g. Rafikov 2005; Rice, Lodato & Armitage 2005). Hydrodynamical simulations show that these planets migrate inward very rapidly in massive discs (e.g. Vorobyov & Basu 2006; Boley et al. 2010; Baruteau, Meru & Paardekooper 2011), perhaps explaining (Humphries et al. 2019) why wide-orbit separation gas giants are so rare in direct imaging surveys (Vigan et al. 2012; Chauvin et al. 2015). On the other hand, planet–planet scatterings may allow some GI planets to survive on wide orbits (Vigan et al. 2017), especially if the primordial disc is dispersed rapidly. For the early massive protoplanetary discs, the primary time-scale on which its mass is lost (Clarke, Gendrin & Sotomayor 2001) is the viscous time,

$$t_{\text{visc}} = \frac{1}{3\alpha \Omega_K} \frac{R^2}{H^2} = 5.4 \times 10^4 \text{yr} \, \alpha^{-1} \text{yr}, \quad (26)$$

where $\alpha = (\alpha/0.1)$ and the estimate is made at $R = 51.5$ AU. Numerical simulations show that the $\alpha$ parameter due to self-gravity of the disc may reach values of order $\sim 0.1$ in early massive discs (Gammie 2001; Rice et al. 2005; Haworth et al. 2020), and even $\alpha \sim 0.2$ in the magnetized discs (Deng et al. 2020). Additionally, disc depletion due to external photoevaporation may be faster than previously thought (e.g. Haworth & Clarke 2019).

For the case at hand we must require that the primordial gas disc is long gone in TW Hydra. This is because the migration time-scale of a GI planet with mass initially exceeding $1 \, M_\odot$ would be much shorter than 10 Myr. Indeed, if the planet did not open a gap and migrated in the type I regime then its migration time is less than 1 Myr even for a disc as low mass as a few $M_\odot$. If, on the other hand, the planet did open a wide gap and migrated in type II then the migration time-scale is (e.g. Lodato & Clarke 2004)

$$t_{\text{mig2}} \approx \frac{M_p}{M_*} \sim 10^6 \text{yr}, \quad (27)$$

where we used $M_p \sim 2 \, M_\odot$ (this will be justified later) and $M_* \sim 2 \times 10^{-9} M_\odot \text{ yr}^{-1}$. Therefore, the planet would have been long lost into the star if the disc was there for the last 10 Myr.

We emphasize the distinction with the CA problem setting discussed in Section 7 brought about by the different planet formation mechanisms. In the CA scenario the planet does not need to be born at $t = 0$. As is well known, in the classical CA model massive cores are most likely to be made at late times, e.g. at $t \sim 5–10$ Myr (Ida & Lin 2004b; Mordasini et al. 2012a) since the process of core growth is slow. Further, due to its lower mass the type I migration time-scale is longer. Therefore, there is no reason to demand a complete disappearance of the primordial gas disc before the planet disruption commences in the CA framework.

8.1.2 Why did the planet not collapse in 10 Myr?

GI planets are born extended, with their radius $r_p \sim 1$ a few AU, and cool: their central temperature is in hundreds of K (e.g. Helled, Podolak & Krotetz 2008). If dust growth inside the GI planet is neglected, then it cools, contracts, and eventually collapses dynamically when the endothermic reaction of H$_2$ molecule dissociation absorbs a vast amount of thermal energy of the planet (Bodenheimer 1974). The collapse terminates in formation of a planet that is $\sim$ Million times denser, with radius $R \sim 2 R_\odot$ and an effective temperature of 1000 to 2000 K. This luminous post-collapse state is often called the ‘hot start’ of gas giant planets (Marley et al. 2007). Similar to the post-collapse gas giant CA planets, the post-collapse GI planets are unlikely to lose mass at $\sim 50$ AU from the star.

Hence we must demand that the planet remains in the pre-collapse state before the onset of the mass-loss. This is surprising given the age of the system. The evolution from birth to collapse (hot start) is usually thought to be very fast. This result is rooted in the pioneering work of Bodenheimer (1974) who found planet collapse time-scales $\lesssim 0.5$ Myr for $M_p = 1 \, M_\odot$, and even shorter for higher mass planets.
However, the collapse time-scale is sensitive to the dust opacity model used. More recent dust opacity calculations (e.g. Semenov et al. 2003; Zhu, Hartmann & Gammie 2009; Woitke et al. 2016) indicate that dust opacity may be higher by up to a factor of ∼3 at $T \sim 10$–30 K (the effective temperature of GI protoplanets) compared to the opacity employed in the 1980s (e.g. Pollack, McKay & Christofferson 1985; see Appendix A). We find that these higher dust opacities lengthen the duration of the pre-collapse phase by a factor of 5–10. Further, 3D simulations of GI planets immersed in protoplanetary discs show that these planets accrete pebbles very rapidly and become significantly enriched in dust (Boley & Durisen 2010; Boley, Helled & Payne 2011; Humphries & Nayakshin 2018; Baehr & Klahr 2019; Vorobyov & Elbakyan 2019). Putting these factors together we find that metal rich $M_p \lesssim 2 M_J$ gas giants may spend as long as 5–10 Myr in the pre-collapse configuration (see Appendix B and Fig. 9).5

5This conclusion holds as long as grain growth and settling do not deplete $a \lesssim 100 \mu m$ population of grains. At higher grain sizes, Rosseland mean dust opacity may drop (cf. Fig. A1). In that case higher Z planets may actually cool more rapidly (Helled & Bodenheimer 2011).

8.1.3 GI planet disruption by a core

A number of authors have shown that pre-collapse GI planets may develop massive solid cores via grain growth and sedimentation (Kuiper 1951; McCrea & Williams 1965; Boss 1998; Helled & Schubert 2008; Boley et al. 2010; Cha & Nayakshin 2011; Nayakshin 2011; Vorobyov & Elbakyan 2019). The time-scales on which the core grows are a minimum of thousands of years but may be much longer, depending on convection and grain material/growth properties, such as $v_0$ (Helled et al. 2008). If the core grows more massive than $\sim 10 M_{\odot}$, then the energy release during its formation can be too large for the pre-collapse planet – its envelope expands and is eventually lost (Nayakshin & Cha 2012; Nayakshin 2016; Humphries & Nayakshin 2018). This scenario for the core-initiated disruption of GI protoplanets is physically analogous to how cores of AGB stars eject their envelopes except for the energy source – the gravitational potential energy rather than the nuclear energy of the core – and the physical scales of the systems.

At present, there exists no stellar/planet evolution code that takes into account all the relevant physics that we wish to explore here. For example, Helled et al. (2008), Helled & Bodenheimer (2011) present models of grain growth and sedimentation in pre-disruption isolated planets cooling radiatively. Vazan & Helled (2012) investigate how external irradiation affects contraction of these planets. These studies did not include the effects of the massive core energy release on to the planet, which is central for us here. On the other hand, Nayakshin (2015, 2016) include grain growth, sedimentation, core formation, and the effects of the core energy feedback on to the envelope, but use a simplified follow-adiabats approach to model radiative cooling of the envelope, and a simpler equation of state than Vazan & Helled (2012) do. Further, the opacities used by the two codes are different.

Here we shall use the code of Nayakshin (2016) to understand the physical constraints on the pre-disruption planet mass, metallicity, and the mass of the core responsible for the planet disruption. These constrains will be seen to place significant limitations on the disrupted GI planet scenario (e.g. the planet mass is unlikely to exceed $\sim 2 M_J$). In Appendix B we compare for the first time the results of uniform planet contraction calculations (no dust sedimentation allowed) computed with this code with that of the proper stellar evolution model of Vazan & Helled (2012) at the same (Pollack et al. 1985) dust opacity. We find that the difference in the planet collapse time-scale computed by the two codes is within a factor of two, which we deem sufficiently close given the much larger dust opacity uncertainties (Section A).

The thick dashed curves in the top panel of Fig. 9 show the evolution of the radius $r_p$ of a $2 M_J$ planet circling the star with TW Hydra properties at 60 AU for different planet metallicities, from $Z = 1$ (in units of $Z_{\odot}$) to $Z = 12$. All the models start with the central planet temperature of 200 K, the uniform composition and an initial grain size of $a = 0.01 \mu m$. The Zhu et al. (2009) opacity table is used for this calculation. The dust opacity is assumed to be proportional to the metallicity $Z$ of the envelope. The bottom panel of Fig. 9 presents the core mass versus time. The grain breaking velocity is here set at $v_{br} = 5 m s^{-1}$. The thin curves in the top panel show the same calculations but where grain growth and core formation are artificially suppressed.

Fig. 9 shows that at Solar metallicity, $Z = Z_{\odot}$, the planet contracts and collapses by $t \approx 1$ Myr, whether core formation is allowed or not. The planet evolutionary time-scale increases as the metallicity of the planet increases, and so does the core mass. Formation of the core in the planet speeds up evolution of the planet in all the
cases. This occurs due to a lower dust opacity in the envelope as some of the dust settles and gets locked in the core. At the lower metallicities in the figure, the core masses are relatively low, so the effect of the core formation is negligible save for the dust opacity reduction. However, for metallicities \( Z \geq 8Z_\odot \) the core mass exceeds \( 20 M_\odot \). The gas envelope starts to expand soon after this mass is reached and is eventually unbound. For the \( Z = 8Z_\odot \) model, the envelope is disrupted at about \( 8 \text{ Myr} \) in this calculation. A higher metallicity planet meets its end sooner, at about 4 Myr, as its core is more massive and more luminous.

We have found that planets more massive than \( \sim 2 M_\oplus \) are not likely to be disrupted by their cores. This comes about due to two factors. First of all, even at a fixed bulk composition, more massive planets contract much more rapidly, shortening the time window for the core growth (this effect exists whether the core feedback is included or not, see, e.g. Helled et al. 2008). Secondly, observations (Miller & Fortney 2011; Thorngren et al. 2016) show that more massive planets are less metal enriched than their less massive cousins. Simulations of pebble accretion on to gas giant planets (Humphries & Nayakshin 2018) also lead to the same conclusion. The dust opacity of the massive planets is hence expected to fall with planet mass, exacerbating the challenge of assembling a massive core and disrupting the planet with it.

### 8.2 Deposition of matter in the secondary disc: methodology

There are several free parameters in this model (just like for the model in Section 7) which we constrain by trial and error. In the beginning of the calculation, we specify the initial planet mass, \( M_{\text{pi}} \), and the starting position of the planet, \( R_{\text{pi}} \). As per Section 8.1.3, we use a GI planet with initial mass \( M_{\text{pi}} = 1.5 M_\oplus \). By experimenting, we found that the disc viscosity parameter \( \alpha = 2.5 \times 10^{-2} \) results in gas accretion rate similar to the one observed in this feedback. Similarly, setting \( R_{\text{pi}} = 56 \text{ AU} \) resulted in the planet remnant being stranded at 51.5 AU; the planet initial bulk metallicity of \( Z = 6Z_\odot \) gave the right ALMA luminosity for the disc.

We assume that at the time of disruption the planet contains a massive solid core or at least a region so metal rich that it survives the disruption of the hydrogen-rich atmosphere. We refer to the final planet mass as simply the core, and it is set to \( M_c = 0.03 M_\oplus \approx 10 M_\oplus \) for definitiveness here. The part of the planet that is lost and injected into the protoplanetary disc is termed the ‘envelope’, and its mass is \( M_e = M_{\text{pi}} - M_c \).

The mass-loss rate, \( M_p(t) \), is not known a priori. As for binary stars undergoing mass exchange (e.g. Rappaport, Verbunt & Joss 1983; Ritter 1988), it is a function of the planet internal structure and its orbital evolution that in itself depends on the planet–disc interaction and the mass-loss rate (see Nayakshin & Lodato 2012). Such a fully self-consistent calculation is beyond the scope of this paper, and we instead specify the planet mass-loss rate:

\[
M_p = \begin{cases} 
\frac{-M_{\text{inj}}}{\tau_{\text{inj}}}, & \text{for } M_p > M_c, \\
0, & \text{otherwise}
\end{cases}
\]

\[
(28)
\]

where \( \tau_{\text{inj}} = 10^5 \text{ yr} \). This mass-loss rate is partitioned between that for gas (H and He) and metals (mass fraction \( Z \)), thus

\[
M_g = (1 - Z(M)) M_{\text{tr}}
\]

\[
M_Z = Z(M) M_{\text{tr}}.
\]

\[
(29)
\]

In general we do not expect the envelope to have a uniform composition, \( Z(M) \), since dust is of course able to sediment down through the gas. Hence we expect \( Z(M) \) to be a function that decreases from the maximum in the core, which we simply set \( Z(M_p < M_c) = 1 \), to some minimum. For definitiveness, we choose this functional form:

\[
Z(M) = (1 - Z_\infty) \exp \left( -\frac{M - M_c}{M_g} \right) + Z_\infty, \text{ for } M \geq M_c.
\]

\[
(30)
\]

The parameter \( M_{\text{tr}} \ll M_c \) describes how large the metal rich region in the centre of the planet is, and \( Z_\infty \) is the metallicity at the outer reaches of the envelope where the term \( \exp \left( -\frac{M - M_c}{M_g} \right) \approx 0 \) as we use \( M_{\text{tr}} \ll M_c \). In practice, we specify the mean metallicity of the planet envelope, \( Z_e \) and \( M_{\text{tr}}, \text{ from which } Z_\infty \text{ is computed. For the calculation presented in Section 8.3, } M_{\text{tr}} = 0.03 M_\oplus \).

The dust and gas lost by the planet are deposited in a Gaussian ring around the planet location, as described by equation (24). The normalization constant \( C \) ensures that the mass injection rate into the disc is equal to the planet mass-loss rate (equation 28). As per equation (29), the injected mass is split into gas and dust.

### 8.3 Numerical results

Fig. 10 shows the gas and dust surface densities, \( \Sigma \) and \( \Sigma_{\text{dust}} \), at several different times during the calculation. The vertical lines of the same type show the respective positions of the planet.

The gas surface density (thin lines) evolution shows the dominant features of the well known viscous ‘spreading ring’ calculation modified by the continuous mass-loss from the planet. The gas spreads quickly all the way to the star and to \( R \approx 200 \text{ AU} \), as required by the observations of gas accretion and the large extent of the gas disc in TW Hydra (cf. Section 2). Despite a continuous mass injection into the disc, the planet manages to make a depression in

![Image](https://example.com/image.png)
the gas surface density profile around its orbit due to gravitational torques acting from the planet on to the gas. This effect is noticeable while the planet mass is in the gas giant planet regime. By torques acting from the planet on to the gas surface density profile around its orbit due to gravitational forces.

The thicker lines show the dust surface density profile at the respective times. We see that initially the dust surface density is narrower than that of the gas, but eventually the dust spreads. This appears because gas flows inward towards the star inside the orbit of the planet, and outward outside the orbit.

The thicker lines show the dust surface density profile at the respective times. We see that initially the dust surface density is narrower than that of the gas, but eventually the dust spreads. This appears because gas flows inward towards the star inside the orbit of the planet, and outward outside the orbit.

Figure 11. Same as Fig. 4 but now for the GI model (Section 8.3) at \( t = 6.8 \times 10^4 \text{yr} \).

As found by Tsukagoshi et al. (2019), the excess has a radial half width of \( \sim 0.5 \text{AU} \) and an azimuthal half-width of \( \sim 2.2 \text{AU} \). The disc pressure scale height for TW Hydra is \( H \sim 3.5 \text{AU} \) at separation of \( 51.5 \text{AU} \), and thus the observed feature is significantly smaller than \( H \). We note that this immediately implies that the disc (but not necessarily the feature) is optically thin at 51.5 AU. This is because photons emitted from the disc mid-plane perform a random walk in an optically thick disc until they escape vertically out of the disc. Therefore, an image of a point source placed in the mid-plane of such a disc would be broadened by \( \sim H \) at least. This forms an independent confirmation, in addition to the arguments spelled out in Section 5.2 that TW Hydra’s disc is optically thin and thus the rollover in \( \Sigma_{\text{dust}} \) observed behind the T19 feature could not be due to the disc becoming optically thin at this radius.

9.2 A vortex or a circumplanetary disc?

Vortices (e.g. Li et al. 2001) have been suggested to trap dust material in the protoplanetary discs and thus produce bright excess in the dust continuum emission (Baruteau & Zhu 2016). Furthermore, vortices are azimuthally elongated structures, with axial ratio \( \sim 4-6 \) (Richard, Barge & Le Dizès 2013), exactly as observed. However, the radial half-width of vortices is at least \( H \), and likely \( \sim 2 \times \) twice that (e.g. fig. 3 in Lin 2012). For the same reason a vortex would also look much more extended in the azimuthal direction (see fig. 4 in Baruteau & Zhu 2016) than observed. Just like with a gap edge created by a planet, we expect a hole in the dust density distribution inward of the vortex (fig. 10 in Baruteau & Zhu 2016), which is not observed.

Circumplanetary discs are believed to be at most \( \sim 1/3 \) (Bate et al. 2003; Ayliffe & Bate 2009), and more likely 1/10 of the planet Hills radius, as shown by the more recent higher resolution calculations (Wang et al. 2014; Ormel et al. 2015b). Thus, the planet would have to exceed the mass of \( \sim 1.5 M_{\oplus} \) to account for just the radial size of the feature. This does not account for the much larger azimuthal extent of the T19 excess emission. Such a high planet mass would produce a noticeable gap at the disc gas surface density and the dust intensity profile near the planet even for disc viscosity as high as \( \alpha = 0.025 \). This is not observed. Finally, Tsukagoshi et al. (2019) also points out that the total flux from the circumplanetary disc is insufficient to account for the total flux in the feature.

9.3 The dust trail of a planet losing mass

Here we consider the dynamics of grains lost by a low mass planet on a circular orbit embedded in a laminar gas disc around it. The different dust models used in these studies. The standard DIANA dust opacity (Woitke et al. 2016) are higher by a factor of a few than that used by Andrews et al. (2016), Hogerheijde et al. (2016). Although we use the public DIANA opacity code to compute our dust opacities here, we use the standard \( a^{-3.5} \) dust size distribution whereas Woitke et al. (2019) found that \( a^{-4} \) power law was a better fit in their modelling.

9 THE ALMA IMAGE OF T19 FEATURE

Here we discuss the implications of the 2D morphology of the excess emission observed by Tsukagoshi et al. (2019). We use these as additional probes of the scenarios explored in this paper.

9.1 The disc is optically thin

As found by Tsukagoshi et al. (2019), the excess has a radial half width of \( \sim 0.5 \text{AU} \) and an azimuthal half-width of \( \sim 2.2 \text{AU} \). The disc pressure scale height for TW Hydra is \( H \sim 3.5 \text{AU} \) at separation of \( 51.5 \text{AU} \), and thus the observed feature is significantly smaller than \( H \). We note that this immediately implies that the disc (but not necessarily the feature) is optically thin at 51.5 AU. This is because photons emitted from the disc mid-plane perform a random walk in an optically thick disc until they escape vertically out of the disc. Therefore, an image of a point source placed in the mid-plane of such a disc would be broadened by \( \sim H \) at least. This forms an independent confirmation, in addition to the arguments spelled out in Section 5.2 that TW Hydra’s disc is optically thin and thus the rollover in \( \Sigma_{\text{dust}} \) observed behind the T19 feature could not be due to the disc becoming optically thin at this radius.

Figure 11 shows the resultant disc emissivity profile in the three wavelengths in the top panel and the disc properties in the bottom panel. The model fits the data reasonably well except for the rollover, which is too sharp, just like the model in Section 7.2. This model is optically thicker than that used by Andrews et al. (2016) and also smaller than the roll-over in \( \Sigma_{\text{dust}} \) observed behind the T19 feature could not be due to the disc becoming optically thin at this radius.
most likely physical origin for a dust particle outflow from a planet is a thermally driven gas outflow that picks and carries the dust with it. The dynamics of grains in the planet vicinity, at radii between the planet radius and the Hills radius, \( r_p \ll R_H \), clearly deserves a separate detailed investigation which is outside the scope of this paper. Here we are concerned with how the flow may manifest itself to ALMA on scales of much larger than \( r_p \). We perform a 2D calculation of dust particle orbits assuming their trajectories lie in the mid-plane (note that \( R_H \ll H \) for a low mass planet).

The dust particle size at the outflow is likely to be much smaller than the mm-sized particles that ALMA sees in TW Hydra’s disc. This is because the inner region of the planet is expected to be sufficiently hot to vaporize even the most refractory dust (Brouwers et al. 2018). This is relevant because for both the CA and GI planet losing mass scenarios the time when the model fits the data best is close to the end of the mass-loss phase from the planet, when the most central regions of the planet are lost into the disc.

As the outflow leaves the planet, the gas density drops, and so does its optical depth. Due to adiabatic expansion and radiation (the outflow eventually becomes transparent to radiation) the gas temperature drops with distance from the planet and the metals condense into dust particles. The grains then grow rapidly. In the disc geometry, the grain growth time scale is \( \tau_{\text{grow}} \sim (1/\Omega_K)(\Sigma/\Sigma_{\text{dust}}) \) (Birnstiel et al. 2012). For the gas just lost by the planet the gas-to-dust ratio is not very large as the planet central regions are very metal rich in our model, therefore \( \tau_{\text{grow}} \) may be expected to be of order a few orbital times in the disc, \( 2\pi/\Omega_K \).

The dynamics of dust particles is most sensitive to the Stokes number, \( St \), and hence we reformulate the problem in its terms. The dust particles are ejected by the planet with initial Stokes number \( St_{\text{min}} = 10^{-3} \), and grow to a maximum size corresponding to the maximum Stokes number of \( St_{\text{max}} = 0.1 \). We describe the particle growth process as a time-dependent \( St \) number

\[
\ln St = (1 - q^*) \ln St_{\text{min}} + q^* \ln St_{\text{max}},
\]

where \( q = t/(t_{\text{grow}} + t) \), where time \( t \) counted from the time the grain was ejected by the planet, \( t_{\text{grow}} = N_t/(2\pi/\Omega) \) is the growth time-scale, with \( N_t = 4 \). For reference, \( St = \sqrt{St_{\text{min}} St_{\text{max}}} = 0.01 \) at \( t = t_{\text{grow}} \).

The planet is assumed to be of a sufficiently small mass that we can neglect its dynamical influence on the surrounding gas. Similarly, we neglect the planet physical size compared with the scales of interest, assuming that dust is emitted from a point (planet position). The planet is on a circular orbit around the star at \( R = 51.5 \) AU. We integrate the standard 2D equations of motion for individual dust grains lost by the planet. Grains are ejected by the planet at a steady rate. As expected, the grains are blown inward by the radial drift and eventually disappear into the star but here we are interested in the dust particle morphology in the immediate vicinity of the planet to compare to the T19 ALMA image of the excess emission region.

The left-hand panel of Fig. 12 shows the location of the dust particles integrated as described above. The coordinates are centred on the planet which is on a prograde circular orbit that follows the dashed circular path. We observe that the dust particles perform a U-turn as seen from the planet location. Since initially the dust particles are small (\( St \ll 1 \)), they are very tightly coupled to gas at \( t \ll t_{\text{grow}} \). In the frame of the planet they start to lag behind the planet because the dust is picked up by the gas in the disc and so travels with the velocity

\[
v_{\text{gas}} = v_K \left( 1 - \frac{H^2}{R^2} \right)^{1/2} < v_K,
\]

which is smaller than the planet orbital speed \( v_K \). However, as the dust particles grow, they start to drift inward of the planetary orbit. When the dust particle drifts to radius \( R < R \) such that its angular speed there exceeds that of the planet, that is, \( v_{\phi}(R)/R > v_K(R)/R = \Omega_K(R) \), it starts to orbit around the star faster than the planet. Hence the particle overtakes the planet eventually.
This orbital motion of the dust looks like a tight U-turn around the planet. Additionally, as the particle sizes grow as they move farther and farther away from the planet, the speed differential between the planet and the dust particles increase. This leads to dust particles spending more time in the U-turn region than in the region in front of the planet. The dust density is hence larger in close proximity to the planet and decreases with distance along the dust tail.

The right-hand panel of Fig. 12 shows a simulated ALMA image of the dust dynamics smoothed by the ALMA beam for TW Hydra. We added a point source to the planet location and a uniform background. We see that the U-turn of the dust produces an emission feature elongated in the azimuthal direction, somewhat analogous to the observations shown in Fig. 1. The exact brightness of the extended tail compared to the U-turn region, the pitch angle of the tail with respect to the azimuthal direction, and the length of the U-turn region do depend on the parameters on the dust growth model used. However, a good qualitative match to the shape of the Tsukagoshi et al. (2019) excess emission is obtained for a wide range of model parameters, not requiring fine tuning. The weak excess emission in the dust tail running in front of the planet and pointing inward of its orbit is a unique testable prediction of our model.

10 DISCUSSION

TW Hydra hosts a protoplanetary disc resolved by ALMA with a record breaking resolution of about 2 AU. The disc has a cliff-like rollover beyond about 50 AU and a significant excess emission resolved by ALMA into a blob with sizes ~1 AU radially by ~4 AU azimuthally. The excess is suspected to be a young planet and is located at 51.5 AU, right at the edge of the dust disc. The protostar continues to accrete gas at a respectable rate of ~2 × 10^{-4} M_⊙ yr^{-1} despite being one of the oldest protostars known (~10 Myr old). Furthermore, its dust disc is nearly two orders of magnitude more massive than the median for Class II sources (Williams et al. 2019), most of which are younger than TW Hydra. Here we have shown that we can use these known and unique properties of the system to constrain scenarios of the protoplanetary disc evolution.

10.1 The quasi-steady state scenario

In this scenario (Section 5) the protoplanetary disc in TW Hydra is primordial, e.g. ~10 Myr old. Previous work (e.g. Powell et al. 2019) and analytical arguments on the presence of ~ mm-sized dust in the disc (Section 3.3), and the observed gas accretion rate (Section 3.2), require the gas disc mass M_d to exceed ~0.1 M_⊙ in this case. We found this scenario to be challenged by the data and other results in the field:

(i) The observed cliff-like rollover in the dust continuum emission beyond ~50 AU is very puzzling for such an old disc that is known to extend to ~200 AU in CO and other molecular tracers. Numerical experiments (Section 5.2) and analytical arguments (Section 3.5) show that one expects a power-law like decline in Σ_dust with radius in this case. We found that the scenario may produce a sharp break in the disc emissivity if the disc becomes optically thick inside 50 AU (Fig. 4). However, for TW Hydra this overpredicts the total flux from the disc by a factor of ~3, contradicts earlier conclusions from photometry data (Section 5.2), and the relatively small size of the Tsukagoshi et al. (2019) feature (Section 9.1). All of these observations require an optically thin disc in the ALMA bands. Further, this model disc becomes optically thin at longer wavelengths and hence predicts a steep decline in the disc intensity with radius at ~50 AU, whereas the 9 mm EVLA data show a very gradual decline in that region (blue curves in Fig. 4).

(ii) The presence of planets. Mentiplay et al. (2019) inferred the masses of M_p ~ 4 M_J for the two putative planets located inside the observed gaps at 24 and 41 AU. Tsukagoshi et al. (2019) estimated the planet mass at 51.5 AU to be M_p ~ 1 Neptune masses. The type I migration time-scale for these planets is ~1 to a few percent of TW Hydra age (Section 3.6). To observe even one of these three putative planets, we need to be quite lucky. To observe all three of these planets, we need to postulate that they were all born essentially simultaneously. This is unlikely because the rates of planet embryo assembly are strongly separation-dependent (Ida & Lin 2004a; Mordasini et al. 2012b; Lambrechts, Johansen & Morbidelli 2014; Ndugu et al. 2019).

(iii) The association of the Tsukagoshi et al. (2019) feature with the dust disc rollover. Planets are expected to block the inward flow of dust, producing gaps at the location of the planets, and bright rings just beyond the gaps (Rice et al. 2006; Pinilla et al. 2012; Dullemond et al. 2018; Zhang et al. 2018). Our numerical experiments in Section 5.1 confirmed these well known results. These dust emission characteristics are not observed in TW Hydra, where the emission plunges instead of rising beyond the planet location.

(iv) The size and shape of the extended excess emission detected by Tsukagoshi et al. (2019). The half-sizes of the feature at 1.3 mm continuum is ~2.2 AU in the azimuthal direction and ~0.5 AU in the radial emission. This extent is too small for a vortex but too large for a circumplanetary disc of a Neptune mass planet (Section 9.2). Increasing the planet mass above 1 M_J may result in the disc large enough but its elongation along the azimuthal direction by a factor of 4 contradicts numerical simulations of circumplanetary discs which show no such elongation (Ayliffe & Bate 2009; Szulágyi et al. 2014; Wang et al. 2014; Omel et al. 2015a). Additionally, such a high mass planet is ruled out based on the protoplanetary dust disc morphology as explained in (iii).

(v) A very small disc viscosity. The observed gas accretion rate on to the star is surprisingly low if the disc mass is really as high as 0.1 M_⊙, and requires the disc viscosity parameter α ≲ 10^{-4} (see Section 3.3). The results of modelling ALMA observations of other bright discs with annular gaps and rings show that for particle sizes a ~ 2 mm the disc viscosity parameter must be larger than ~10^{-3} (fig. 7 in Dullemond et al. 2018).

(vi) Surprisingly small grains. Analytical arguments (Section 3.4) and numerical models show that if a disc is massive as 0.1 M_⊙ the grains should grow rapidly to sizes much larger than ~1 mm, and be lost into the star too soon, unless the dust fragmentation velocity is ~0.3 m s^{-1}. The latter value is significantly lower than the values obtained in laboratory experiments (e.g. Blum & Wurm 2008) and ~10 m s^{-1} typically used in the protoplanetary disc literature (e.g. Birnstiel et al. 2012; Drążkowska et al. 2014; Rosotti et al. 2019).

(vii) Dusty rings rather than spirals. Veronesi et al. (2019) show for TW Hydra and other ALMA discs that gas discs can be ‘weighted’ by understanding the response of the mm-sized grains to the planets embedded in these discs. They find that in massive discs the mm-sized grains would tend to be in spiral features driven by the planets, whereas in low mass gas discs they would conform to the shape of rings. Based on the absence of spirals and presence of rings the authors conclude that the disc masses are ~1 M_J.

(viii) Oddity compared to other discs. The dust mass of TW Hydra is extraordinarily large. Using the pre-DMANA opacity model,
this mass is estimated at $\sim 80$ $M_\oplus$ (Andrews et al. 2012, 2016). The mean dust mass of class 0 sources was recently estimated at 26 $M_\oplus$ (Tobin et al. 2020); these sources are a factor of $\sim 100$ younger than TW Hydra. The more comparable yet still younger by a factor of several class II discs have dust disc masses almost 2 orders of magnitude lower than that of TW Hydra (Williams et al. 2019). Using DIANA (Woitke et al. 2016) opacities we find a factor of $\sim 6$ lower dust mass for TW Hydra; however all the other results cited above should then be scaled down as well, leaving TW Hydra’s dust mass excess just as large.

10.2 The phenomenological planet losing dust scenario

In Section 6 we used the same massive disc scenario as discussed in Section 10.1, but assumed that the protoplanetary disc is dust-free before a source of dust of unspecified nature starts ejecting dust. This produced a better match to the data, resolving qualitatively the problems listed in (i). Large dust particles drift inward, naturally explaining why the T19 feature is positioned at the dust disc rollover, alleviating (iii). However, the model violates mass conservation and second Newton’s law, and does not resolves the other challenges from Section 10.1.

10.3 A core accretion planet losing dust

We argued in Section 7.1 that a massive core can lose its pre-collapse massive dusty gas envelope if a catastrophic release of energy occurs in its core, due to e.g. a merger of the core with another massive core. We dropped the assumption of a massive gas disc, which becomes unnecessary if the dust in the protoplanetary disc of TW Hydra is of a recent rather than primordial origin. In the particular example of the numerical calculation in Section 7.2 we considered a pre-collapse planet of the total initial mass of 38 $M_\oplus$, to lose its half dust/half gas envelope (planet metallicity $Z = 0.5$) until its mass dropped to 10 $M_\oplus$, at which point the mass-loss was turned off. The initial disc mass was set at 0.002 $M_\odot$, which required disc viscosity of $\alpha = 0.02$ to yield the correct gas accretion rate on to the star.

This vastly improved the results, resolving all issues (i)–(viii), e.g. producing a reasonable match to the observed spectra with a now reasonable value for the grain fragmentation (breaking) velocity, $v_{br} = 10$ m s$^{-1}$, a value of $\alpha$ in accord to the constraints from DSHARP modelling (Dullemond et al. 2018). Due to the much lower gas disc mass, the planet migration time is comparable to the age of the system, not requiring a miracle of several planets being born at the same time. The Stokes number of mm-sized grains satisfied the Veronesi et al. (2019) constraint. A disruption of a massive pre-collapse planet via a catastrophic collision with another planet is not likely to be a common outcome for the core accretion scenario, and this may explain why TW Hydra is such an oddity (viii). Recently, Demidova \& Grinin (2019, APJ, 887, Issue 1, article id. L15) showed that catastrophic collision of planetary embryos in a protoplanetary discs releases enough dust to be observable with ALMA.

10.4 A gravitational instability planet disruption

In Section 8 we considered a disruption of a gas giant planet formed by the GI scenario. Since GI planets are presumably born in very young, class 0/I discs, this planet would have survived at such a wide orbit only if the disc was dissipated very rapidly in this system (Section 8.1.1). This therefore requires that TW Hydra had no protoplanetary disc before the planet disruption. It is also possible that there were more GI planets early on, and that one of them was scattered on a wider orbit than the rest, boosting its chances of survival far out.

Just as with the core accretion planets, the pre-collapse GI planets are extended and are susceptible to their envelopes being destabilized if enough energy is injected into the planet centres. Massive solid cores ($M_{\text{core}} \gtrsim 10 M_\oplus$) were previously shown to be capable of disrupting the planet envelopes (e.g. Nayakshin \& Cha 2012; Nayakshin 2016; Humphries \& Nayakshin 2018). For a very old system such as TW Hydra, we found that only very metal rich ($Z \sim 0.1$) GI planets with masses no larger than 2 $M_\oplus$ can be disrupted via this mechanism at $t \sim 10$ Myr (Section 8.1.2 and Section 8.1.3).

In Section 8.3 we found that disruption of a planet with an initial mass $M_p = 1.5 M_\oplus$, initially orbiting TW Hydra at 56 AU resulted in a gas disc quickly spreading both inward, to fuel gas accretion on to the star at rates close to those observed in the system, and outward to $\sim 200$ AU. As with the CA planet losing dust scenario, the dust lost by the planet grows to mm sizes and then streams only inward of the planet due to the aerodynamical friction with the gas.

Although the physics of the models differs, the two scenarios give equally promising explanations for the observed spectra of the source and yield attractive explanations to all the points (i) – (viii) raised as difficulties of the standard quasi-steady-state scenario.

10.5 The dust morphology of the T19 excess emission source

Finally, we investigated the dynamics of dust grains lost by a low mass planet in 2D in Section 9. We argued that dust particles must be carried away from the planet by a gas outflow, and must therefore be microscopic initially. We then argued that when released into the disc the dust will grow to larger sizes as constrained by the disc properties. The dust particles were found to perform a U-turn around the planet, first being dragged along by the gas flowing past the planet, but then overtaking the planet a little inward of its orbit when they have grown sufficiently to drift through the gas.

When convolved with the ALMA beam at 1.3 mm this results in an emission excess elongated along the orbit and predicts a weak tail extending in front and a little inward of the planetary orbit.

10.6 Planet-losing mass scenario disadvantages, uncertainties, and future tests

While we found a number of compelling spectral and physical arguments to favour the planet disruption scenarios over the traditional quasi-steady-state framework for disc evolution with planets that only gain mass, there are many issues that need further investigation. First of all, more effort needs to be invested in detailing the conditions under which core accretion and gravitational instability planets can be disrupted with such a significant amount of dust lost as well. For this to be the case, the dust in the envelope must be well coupled to the gas or else it settles into the core, and the envelope would also cool too rapidly and hence collapse. This tight dust–gas coupling is probably natural in the envelope centre where dust may sublime and be in the gas phase anyway, but in the outer regions of the envelope the dust must remain sufficiently small.

One should also aim to constrain the mass-loss rate and parameters such as the outflow speed from first principles. Our 2D dust dynamics calculation in Section 9.3 assumed that gas dynamics near the planet is dominated by the laminar shear flow of gas around the protostar. It is quite possible that 3D hydrodynamical calculations of a gas–dust outflow from a planet in the disc may lead to spiral...
features, which may be very different in nature to those launched by the planet’s gravity. Recent detection of spiral density features in TW Hya disc by Teague et al. (2019) may test this scenario.

Both CA and GI planet disruption scenarios for TW Hya hinge significantly on the dust opacity model used here (Woitke et al. 2016), which predicts opacity larger than much of previous work. Woitke et al. (2016) show that their ‘standard’ opacity is larger than that used by Andrews & Williams (2005) at 850 μm by a factor of 1.6. We further found that to match the normalization of the disc intensity profiles in the three wavelengths simultaneously, an amorphous carbon fraction of 26 per cent is required, which is very close to the 25 per cent fraction found by Woitke et al. (2019) for TW Hya. This yields a further increase by a factor of ∼2–3 in the dust absorption extinction in ∼ mm wavelengths (e.g. see fig. 3, the green curve, in Woitke et al. 2016). As a result, the dust disc mass of TW Hya in our models is only ∼ 15 M⊕, low enough to be accounted for by dust rich envelopes of massive planets.

This contrasts strongly with the results of Ueda, Kataoka & Tsukagoshi (2020) who have recently obtained a dust mass of ∼ 150 M⊕ just inside the inner 10 AU of TW Hya. Extended to the outer dust disc edge, this estimate is two orders of magnitude larger than the values obtained here. Ueda et al. (2020) emphasize the inclusion of dust scattering as the main driver of their much higher dust mass compared with previous literature. However, these effects are also included here via the Zhu et al. (2019) formalism. In fact, all of our reasonably successful fits to TW Hya disc intensity profiles are becoming optically thick inward of 10 AU (cf. Figs 6, 8, and 11), in close agreement with Ueda et al. (2020). The Woitke et al. (2019) calculations also include dust scattering, and their dust mass for TW Hya is similar to ours. Therefore, the more likely source of the disagreement is in the dust opacity model. As an example, Ueda et al. (2020) dust absorption opacity is 65 times lower than ours at the wavelength of 3.1 mm. These differences show that constraining the actual dust opacity in TW Hya would go a long way towards testing our model; if dust extinction opacity is significantly lower than used here then the dust disc mass budget is simply too large to originate from a disrupted planet of any sort.

Further, a detailed chemodynamical modelling of TW Hydra in the context of a disrupted planet scenario is needed to ascertain that it may explain the extremely rich data set for this well observed source (e.g. Andrews et al. 2012; Bergin et al. 2013; Menu et al. 2014; Woitke et al. 2019). Fig. 13 shows the model dust and gas surface density profiles from Fig. 11 that we found to match the observed disc spectra best. These are compared with the broken power-law dust surface density model of Hogerheijde et al. (2016) and the three models for Σ previously shown in Fig. 1.

We see that while the dust surface density match is reasonably good (which of course is the goal of our paper), the gas surface density profile and the total gas disc mass is significantly lower than previous workers assumed or derived. Without sophisticated modelling it is unclear how serious the disagreement is. Since the disrupted planet is metal rich in our scenario, the mass of various molecular species may be sufficiently high in the model to account for their observed emission since previous workers assumed much lower abundances for the disc. However, HD line emission is not expected to be sensitive to the metallicity of the gas (e.g. Bergin et al. 2013; Woitke et al. 2019); it remains to be seen whether our much less massive disc may account for the observed line fluxes.

11 CONCLUSIONS

Here we focused on the first ALMA 1.3 mm dust continuum excess emission (Tsukagoshi et al. 2019) positioned right at the edge of a cliff-like rollover of the dust disc in TW Hydra. We showed that the morphology of the blob-like excess and its relation to the dust disc are best explained by a planet losing dust and gas within the excess. We argued that pre-runaway core accretion planets and pre-collapse gravitational instability planets may be disrupted and may provide the required mass injection into the system. This catastrophic event may also explain why there is a factor of ∼100 more dust in this very old system than the mean for (typically younger) class II protoplanetary discs. Future modelling needs to improve on the internal planet structure, mass-loss dynamics, dust composition and opacity, and chemodynamical modelling.

ACKNOWLEDGEMENTS

The authors thank John Ilee for useful discussions and suggestions. SN acknowledges support from STFC grants ST/N000757/1 and ST/M006948/1 to the University of Leicester. This work made use of the DiRAC Data Intensive service at Leicester, operated by the University of Leicester IT Services, which forms part of the STFC DiRAC HPC Facility (www.dirac.ac.uk). The equipment was funded by BEIS capital funding via STFC capital grants ST/K000373/1 and ST/R002363/1 and STFC DiRAC Operations grant ST/R001014/1. DiRAC is part of the National e-Infrastructure. CH is a Winton Fellow and this work has been supported by Winton Philanthropies, The David and Claudia Harding Foundation. FM acknowledges support from the Royal Society Dorothy Hodgkin Fellowship.

REFERENCES

Alexander R., Pascucci I., Andrews S., Armitage P., Cieza L., 2014, in Beuther H., Klessen R. S., Dullemond C. P., Henning T., eds, Protostars and Planets VI. University of Arizona Press, Tucson, AZ, p. 475

ALMA Partnership et al., 2015, ApJ, 808, L3

Andrews S. M. et al., 2012, ApJ, 744, 162

Andrews S. M. et al., 2016, ApJ, 820, L40

Andrews S. M. et al., 2018, ApJ, 869, L41

Andrews S. M., Williams J. P., 2005, ApJ, 631, 1134

Ayliffe B. A., Bate M. R., 2009, MNRAS, 397, 657

Bachr H., Klahr H., 2019, ApJ, 881, 162

Bai X.-N., 2016, ApJ, 821, 80

Bai X.-N., Stone J. M., 2013, ApJ, 769, 76
APPENDIX A: DUST OPACITY UNCERTAINTIES

Fig. A1 shows several models for the absorption Rosseland mean opacity, $\kappa_R$, of gas at Solar metallicity from several different authors as a function of gas temperature. For temperatures $T \leq 10^3$ K and gas densities typical of pre-collapse planets, $\kappa_R$ is strongly dominated by dust. For this paper, the shaded temperature region, $10 \leq T \leq 30$ K, is most important as this encompasses the expected effective temperatures for our dust-rich wide-separation planets (the energy transfer in deeper hotter planet interiors is dominated by convection anyway; Helled et al. 2008). The two DIANA opacity calculations (Woitke et al. 2016) neglect grain vaporization as this is not important in the shaded region, but include the effects of grain growth, by allowing the maximum grain size to be either 10 or 100 $\mu$m.

We see that there is a factor of about 30 uncertainty between the smallest and the largest $\kappa_R$. This shows that early calculations of giant planet contraction (e.g. Bodenheimer 1974) may have significantly overestimated the luminosity of these objects. Furthermore, higher metallicity objects have proportionally higher dust opacities, further delaying planet contraction.

APPENDIX B: PRE-DISRUPTION PLANET CONTRACTION COMPUTED WITH TWO DIFFERENT CODES

As explained in Section 8.1.3, to model planet contraction simultaneously with dust growth and sedimentation into the core, we use the code of Nayakshin (2016). Here we compare the results of this code, which uses an isentropic (follow-adiabats) approximation to the energy transfer through the planet envelope, to the more accurate stellar evolution model of Vazan & Helled (2012) for the simpler case in which grain growth and sedimentation are neglected. Fig. B1 shows the evolution of planetary radius computed with the two different codes for the same opacity (Pollack et al. 1985) for several planet masses. The evolutionary tracks computed with the two codes are within $\sim 30$ per cent of each other in terms of the absolute value of the planet radius, and within a factor of two in terms of the planet collapse time-scales. We deem this sufficiently close given the much larger uncertainty that exists in the dust opacity.

Figure B1. Comparison of planet radii versus time computed with the codes of Nayakshin (2016) and Vazan & Helled (2012). For each planet mass, the two models are initialized with the same central temperature.

This paper has been typeset from a $\LaTeX$ file prepared by the author.