Relationship between advancing abutment pressure and deformation of surrounding rock in a roadway: A case study in Helin coal mine in China

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Abstract: The deformation stages of the working face of a mine in front of the roadway were defined based on the location of the roadway and the coal wall in different deformation zones. Observational data of the advancing abutment pressure and the surrounding rock deformation of the roadway from Helin coal mine were analyzed using least squares fitting. The results show that the distance between the boundary of the rapid deformation stage and the deceleration deformation stage and the position where the advancing abutment pressure is equal to the original rock stress is 0.8 m. The distance between the boundary of the large deformation stage and the stable small deformation stage and the peak value of the advancing abutment pressure is 0.3 m. A theoretical analysis indicated that the boundary between the rapid deformation stage and the deceleration deformation stage is located at the intersection of the advancing abutment pressure curve and the original rock stress curve. The boundary between the large deformation stage and the stable small deformation stage is located at the peak value of the advancing abutment pressure.

Keywords: Fully-mechanized caving mining; Advancing abutment pressure; Roadway deformation; Relationship between stress and deformation

1 Introduction

As a result of the continuous improvement of coal mining technology and mining equipment in China, large-scale mechanized caving mining has been used widely. The determination of the advancing abutment pressure of fully-mechanized caving mining and the characteristics of the deformation of the surrounding rock in the roadway is of great significance for in-depth studies of mining pressure, roadway support, and equipment selection. Studies of the advancing pressure and
the deformation of the surrounding rock in the roadway following the methods of Qian, Song, and Hou\cite{1,2} have resulted in constructive achievements. Xu\cite{3,4} investigated the influence of the key layer on the characteristics of the mining pressure in a fully-mechanized working face. Wang \cite{5,6} obtained good results in a study of the influence of the caving ratio on the characteristics of the mining pressure in a fully-mechanized working face. Pan and Zhang\cite{7,8,9} determined key rules regarding the characteristics of the mining pressure in different areas and different mines in a fully-mechanized working face. Ma\cite{10,11} conducted in-depth theoretical and experimental research on the stress and failure characteristics of roadways during mining. Kang\cite{12,13} conducted in-depth research on roadway deformation damage and control technology and the methods are widely recognized in the industry. Gou\cite{14,15} investigated the mechanical processes of roadway destruction. However, few studies have been conducted on the influence of the pressure distribution on the roadway deformation and their relationship.

In this paper, a theoretical analysis and field measurements are integrated to investigate the connection between the advancing abutment pressure and the deformation of the surrounding rock in the roadway of a fully-mechanized coal mine; the j7401 working face of the Helin coal mine is used as the example.

2 Overview of the study background

The 7(4) coal seam in the j7401 working face of the Helin coal mine has a surface elevation of $+255 \sim +310$ m, a level elevation of $-150$ m $\sim 270$ m, a length of the working face of 240 m, and an advancing direction length of 1520 m; the inclination range of the working face is larger and the average angle of the working face is about 6°. The range of the coal seam thickness of the working face is 7.8 m $\sim 13.6$ m and the average thickness of the coal seam is about 11.4 m. Because the hardness of the coal seam is relatively low, the stability is low, a 3.4-m mining height and an 8-m top coal caving height are used in the fully-mechanized top-caving coal mining. The overburden structure of the working surface is relatively simple. The top and bottom plate consist of mudstone...
and sandstone and the bottom is carbonaceous mudstone, which is black-gray with a thin, dense, and hard layer and an average thickness of 6.70 m. The old bottom is also black and brown-gray, consists of silty sandstone that is dense and hard with an average thickness of 8.65 m.

3 Theoretical analysis

Due to the existence of a beam structure, a zone of increasing stress is formed in front of the working face as mining progresses, as shown in Figure 1. Prior to the structural failure of the beams, the advancing abutment pressure increases continuously, the surrounding rock of the roadway moves closer, and the moving speed increases. \[1,2,16,17\] During this process, the working face is continuously progressing. Under the influence of the advancing abutment pressure, two areas are formed in front of the working face, i.e., the plastic zone (zone A) and the elastic zone (zone B).

![Fig. 1 Diagram of the advancing abutment pressure](image)

The equation of the hydraulic equilibrium in the horizontal direction and vertical direction at any location in the plastic zone is:

\[
0 = m \sigma_x + 2f \sigma_y d_x - m(\sigma_x + d \sigma_y)
\]

(1)

Where \( m \) is the thickness of the working face, \( f \) is the friction coefficient, \( \sigma_x \) is the horizontal stress of the unit, \( \sigma_y \) is the vertical stress of the unit.

Based on the Mohr-Coulomb criterion, equation (1) is obtained:
\[ \sigma_y = 2C \sqrt{\frac{1 + \sin \psi}{1 - \sin \psi} + \frac{1 + \sin \psi}{1 - \sin \psi}} \sigma_x \quad (2) \]

Where \( C \) is the cohesion of the coal, \( \psi \) is the internal friction angle of the coal.

We define \( R_\psi = \frac{1 + \sin \psi}{1 - \sin \psi} \), \( R_c = 2C \sqrt{\frac{1 + \sin \psi}{1 - \sin \psi}} \)

The vertical stress expression in the plastic zone can be reduced to:

\[ \sigma_y = N_0 e^{\frac{2xR_\psi}{m}}, \quad N_0 \leq \sigma_y \leq k\gamma H \quad (3) \]

Where \( N_0 \) is the supporting capacity of the coal wall, \( k \) is the advancing stress concentration factor.

When \( \sigma_y = k\gamma H \), the advancing abutment pressure reaches its peak and the distance between the peak position and the coal wall, \( x_0 \), is represented as:

\[ x_0 = \frac{m}{2} \frac{1 - \sin \psi}{1 + \sin \psi} \ln\left( \frac{k\gamma H}{C + \sigma \tan \psi} \frac{1 - \sin \psi}{1 + \sin \psi} \right) \quad (4) \]

Where \( \sigma \) is the support resistance to the flank.

The peak of the advancing abutment pressure in front of the working face occurs at \( x_0 \) m and represents the boundary between the elastic deformation area (area B), which is \( x_0 \) m in front of the working face and the plastic deformation zone, which is \( 0 \) to \( x_0 \) m in front of the working face. The plastic deformation zone is divided into the failure zone (zone C) and limit equilibrium zone (zone D) by the intersection of the advancing abutment pressure curve and the original rock stress line.

In zone C, the coal strata that lost its integrity and has poor carrying capacity causes large and sharp deformation of the surrounding rock in the roadway; this is referred to as the rapid deformation stage of the surrounding rock of the roadway. In zone D, although the coal bed has higher integrity and bearing capacity and experiences plastic deformation, it is still in a discontinuous state. There is
less roadway deformation in this area and the rate of deformation is slower; this is referred to as the deceleration deformation stage of the surrounding rock of the roadway. The failure zone and the limit equilibrium zone are collectively called the plastic zone with large deformation; this is called the large deformation stage.

The elastic deformation zone, where the coal rock formation is in good condition and has good bearing capacity is referred to as the stable small deformation stage. Although the roadway deformation is small in this area, it is larger than the deformation of the roadway under the original rock stress.

4 Field test

4.1 Arrangement of the observation stations

4.1.1 Observation station of the advancing abutment pressure

Four groups of observation stations were set up 100 m ahead of the j7401 fully-mechanized working face; each observation covered two boreholes located in the transportation roadway and the ventilation roadway respectively. The depths of the two drilling holes were 3 m in the first group, 6 m in the second group, 12 m in the third group, and 15 m in the fourth group. One borehole stress meter was placed in each borehole and was located 1.5 m from the floor of the mining roadway. The layout of the stress gauges and boreholes in the working face are shown in Figure 2. The observations were conducted based on the progress of the j7401 fully-mechanized working face. The distance between the observation point and the working face lager than 50 m and the observation data were recorded every two days during the morning shift. The distance between the observation point and the working face was 30 to 50 m and the observation data were recorded daily during the morning shift. The distance between the observation point and the working face smaller than 30 m and the observation data were recorded daily during the morning shift and midday shift.
4.1.2 Observation station of the surrounding rock deformation

In the fully-mechanized mining face, the deformation of the back mining roadway was observed to determine the deformation characteristics of the surrounding rock of the transport roadway and the ventilation roadway and analyze the influence of the mining on the surrounding rock deformation. Observation lines with three stations located 30 m apart were laid out in a cross pattern to observe the surface displacement of the mining roadway. The layout parameters of the tunnel test station are shown in Figure 3.

4.2 Results and discussions

4.2.1 Variations in the advancing abutment pressure

As the fully-mechanized caving face is pushed forward, the coal body is gradually deformed and broken and the borehole wall in the mining roadway is filled between the borehole and the
borehole stress gauge. As a result, the borehole stress gauge in the roadway is in full contact with the coal body in the fully-mechanized working face. The measurements of the borehole stress meter from eight boreholes at the four test stations are shown in Table 1 to Table 4.

Table 1 Stress meter observation data from the 3-m borehole

| No. | Distance between measuring point & the working face/m | Transportation roadway stress/MPa | Stress of ventilation roadway/MPa |
|-----|------------------------------------------------------|----------------------------------|----------------------------------|
| 1   | 2.8                                                  | 7.3                              | 5.7                              |
| 2   | 6.3                                                  | 11.5                             | 10.9                             |
| 3   | 9.0                                                  | 23.6                             | 21.2                             |
| 4   | 11.1                                                 | 31.5                             | 29.8                             |
| 5   | 16.2                                                 | 32.3                             | 32.6                             |
| 6   | 19.9                                                 | 34.4                             | 29.4                             |
| 7   | 26.2                                                 | 25.3                             | 26.2                             |
| 8   | 30.2                                                 | 15.2                             | 17.8                             |
| 9   | 40.4                                                 | 17.3                             | 13.9                             |
| 10  | 50.2                                                 | 13.2                             | 11.9                             |
| 11  | 60.3                                                 | 10.0                             | 10.7                             |
| 12  | 70.0                                                 | 10.0                             | 10.2                             |

Table 2 Stress meter observation data from the 6-m borehole

| No. | Distance between measuring point & the working face/m | Transportation roadway stress/MPa | Ventilation roadway stress/MPa |
|-----|------------------------------------------------------|----------------------------------|-------------------------------|
| 1   | 3.1                                                  | 6.2                              | 7.1                           |
| 2   | 7.0                                                  | 14.2                             | 12.7                          |
| 3   | 9.1                                                  | 21.0                             | 27.2                          |
| 4   | 11.1                                                 | 32.2                             | 30.8                          |
| 5   | 16.1                                                 | 34.3                             | 35.2                          |
| 6   | 20.1                                                 | 29.2                             | 24.1                          |
| 7   | 25.3                                                 | 26.2                             | 26.4                          |
| 8   | 30.3                                                 | 17.3                             | 21.5                          |
| 9   | 40.2                                                 | 15.2                             | 19.9                          |
| 10  | 50.3                                                 | 12.2                             | 13.2                          |
| 11  | 60.2                                                 | 10.3                             | 11.0                          |
| 12  | 70.0                                                 | 10.1                             | 10.2                          |
Table 3 Stress meter observation data from the 12-m borehole

| No. | Distance between measuring point & the working face/m | Transportation roadway stress/MPa | Ventilation roadway stress/MPa |
|-----|--------------------------------------------------|---------------------------------|-------------------------------|
| 1   | 2.9                                              | 6.5                             | 5.9                           |
| 2   | 7.1                                              | 17.2                            | 14.1                          |
| 3   | 9.3                                              | 26.2                            | 23.8                          |
| 4   | 10.7                                             | 36.2                            | 33.4                          |
| 5   | 15.3                                             | 37.6                            | 35.9                          |
| 6   | 20.1                                             | 29.3                            | 27.4                          |
| 7   | 24.1                                             | 21.3                            | 24.3                          |
| 8   | 30.1                                             | 20.2                            | 19.7                          |
| 9   | 40.6                                             | 18.2                            | 16.1                          |
| 10  | 50.2                                             | 15.1                            | 12.8                          |
| 11  | 60.0                                             | 12.3                            | 10.7                          |
| 12  | 69.1                                             | 10.1                            | 10.2                          |

Table 4 Stress meter observation data from the 15-m borehole

| No. | Distance between measuring point & the working face/m | Transportation roadway stress/MPa | Ventilation roadway stress/MPa |
|-----|--------------------------------------------------|---------------------------------|-------------------------------|
| 1   | 2.7                                              | 6.3                             | 7.2                           |
| 2   | 7.2                                              | 16.6                            | 13.8                          |
| 3   | 9.0                                              | 26.0                            | 21.7                          |
| 4   | 10.2                                             | 34.3                            | 29.8                          |
| 5   | 15.2                                             | 36.3                            | 36.5                          |
| 6   | 19.2                                             | 30.2                            | 30.7                          |
| 7   | 25.3                                             | 26.3                            | 25.4                          |
| 8   | 30.4                                             | 19.2                            | 21.9                          |
| 9   | 40.7                                             | 16.1                            | 18.7                          |
| 10  | 50.5                                             | 13.1                            | 14.8                          |
| 11  | 59.2                                             | 12.0                            | 11.7                          |
| 12  | 69.7                                             | 10.7                            | 10.3                          |

The borehole stress measurements of the advancing working face at different drilling depths are shown in Figure 4.
Fig. 4 Advancing abutment pressure in different drilling depths

The red line in Figure 4 represents the original rock stress line, the green line represents the transportation roadway pressure, and the blue line represents the ventilation roadway pressure. The following is observed:

(i) When the distance between the fully-mechanized caving and drilling is about 65 m, the borehole stress begins to exceed the rock stress, indicating that the advancing abutment pressure range of the j7401 fully-mechanized working face is about 65 m.

(ii) The peak of the advancing pressure is between 15 m and 22 m in front of the working face, the peak range of the advancing pressure is 33 MPa~39 MPa, and the peak of the advancing
abutment pressure is 3.2~3.8 times that of the original rock stress.

4.2.2 Variations in the surrounding rock deformation

The observation data of the surrounding rock deformation are shown in Table 5 and Table 6. The data were used to determine the influence range of the mining roadway on the fully-mechanized mining face.

| No. | Distance between measuring point & the working face/m | Daily roof subsidence /mm | Daily convergence of both sides/mm |
|-----|-----------------------------------------------------|---------------------------|-----------------------------------|
| 1   | 0.8                                                 | 11.2                      | 11.6                              |
| 2   | 8.2                                                 | 16.2                      | 12.5                              |
| 3   | 10.2                                                | 18.3                      | 7.1                               |
| 4   | 12.6                                                | 16.3                      | 5.3                               |
| 5   | 16.3                                                | 7.2                       | 4.7                               |
| 6   | 19.2                                                | 5.2                       | 3.1                               |
| 7   | 25.1                                                | 2.2                       | 1.0                               |
| 8   | 35.2                                                | 1.2                       | 0.8                               |
| 9   | 45.1                                                | 0.5                       | 0.2                               |
| 10  | 55.2                                                | 0.2                       | 0.2                               |
| 11  | 60.0                                                | 0.0                       | 0.0                               |
| 12  | 70.0                                                | 0.1                       | 0.0                               |

| No. | Distance between measuring point & the working face/m | Daily roof subsidence /mm | Daily convergence of both sides/mm |
|-----|-----------------------------------------------------|---------------------------|-----------------------------------|
| 1   | 0.8                                                 | 9.2                       | 13.2                              |
| 2   | 4.2                                                 | 11.2                      | 14.1                              |
| 3   | 6.5                                                 | 11.4                      | 14.9                              |
| 4   | 10.4                                                | 10.3                      | 11.8                              |
| 5   | 13.7                                                | 8.3                       | 6.1                               |
| 6   | 17.2                                                | 6.2                       | 2.4                               |
| 7   | 20.3                                                | 3.0                       | 3.0                               |
| 8   | 27.0                                                | 2.0                       | 0.8                               |
| 9   | 36.8                                                | 0.9                       | 0.4                               |
| 10  | 49.0                                                | 0.5                       | 0.6                               |
We used the data in Table 5 and Table 6 to plot the velocity changes in the surrounding rock deformation of the transportation roadway and ventilation roadway (Figure 5).

The following results were observed:

(i) In front of the fully mechanized working face, the roof activity is intense at 0~20 m. The maximum daily subsidence rate of the roof is 18 mm in the range of 5-11 m in the front of the working face. The daily convergence of the roof subsidence at 20 m in front of the working face is less than 5 mm for the ventilation roadway and less than 3 mm for the transport roadway. The daily convergence beyond 60 m in front of the working face is close to 0.

(ii) In the range of 0~20m in front of the fully-mechanized working face, the convergence of the two sides is very large. The maximum speed of the two groups of daily convergence at 6 m~8 m in front of the working face is 19.4 mm, and the maximum daily convergence of the two groups is 14.9 mm. The daily convergence values in the range of 20 m–60 m in front of the working face are less than 3 mm. The daily convergence in the front of the working face beyond 60 m is close to 0.

These results indicate that the deformation of the surrounding rock is very large in the range of
0~20 m in the front of the working face, is weak in the range of 20 m~60 m, and the surrounding rock is basically unaffected by mining beyond 60 m.

4.2.3 *Relationship between advancing abutment pressure and roadway deformation*

The changes in the advancing abutment pressure at different positions in front of the fully-mechanized working face were determined using the data shown in Table 1~Table 4 and least squares fitting. The data for the transport roadway and ventilation roadway are analyzed together. The 96 data points in the four tables \((x_i, y_i), \, (i = 1, 2, ..., 96)\) were used to find the approximation function \(y = S(x)\). The principle of this method is to minimize the sum of squares between the fitted value and the actual value to determine the approximation function of \(f(x)\) in \(\Phi = \text{span}\{\phi_0(x), \phi_1(x), ..., \phi_n(x)\}\) (Where \(\phi_i(x)\) is the \(i\) vector function of \(x\)) to find \(a_k (k = 0, 1, ..., n)\).

Let \(S(x) = \sum_{k=0}^{n} a_k \phi_k\) in \(\Phi\) space be the best approximation function for \(f(x)\)\(^{18,19}\).

We used the distance between the measuring point and the working face (Table 1~Table 4) as the independent variable and the advancing abutment pressure as the dependent variable; the fitted function curve is shown in Figure 6.

![Fig. 6 Fitted curve of the advancing abutment pressure](image)

The following is observed in Figure 6:

(i) The advancing abutment pressure gradually increases in the range of 0 m to 19.8 m in the
front of the working face and is equal to the original rock stress at 0.8 m.

(ii) The peak value of the advancing abutment pressure is 39.4 MPa and occurs at 19.8 m in front of the working face.

(iii) The advancing abutment pressure decreases gradually in the range of 19.8~65 m in front of the working face. Beyond 65 m, the pressure is the same as that of the original rock stress.

The data in Table 5 and Table 6 are also analyzed using the least squares fitting method. We made no distinction between the convergences of the two sides and the roof subsidence and considered only the daily roadway deformation. The measuring point and working face distance (Table 5 and Table 6) are used as independent variables and the daily deformation of the roadway in front of the working face is the dependent variable, as is shown in Figure 7.

![Fig. 7 Fitted curve of the daily deformation of the roadway in front of the working face](image)

The following is observed in Figure 7:

(i) The maximum daily deformation occurs at 8.9 m in front of the working face and the daily deformation is larger than 12 mm in the range of 0~8.9 m, which is the rapid deformation stage.

(ii) In the range of 8.9 to 20.1 m the daily deformation of the roadway decreases from 14.5 mm to about 3 mm; this is the deceleration deformation stage.

(iii) The daily deformation of the roadway beyond 20.1 m in front of the working face is very small. The deformation is zero at 65 m. In the range of 20.1~65 m, the daily deformation of the
roadway decreases slowly from 3 mm to 0 mm; this is the stable small deformation stage.

A comparison of the results in Figure 6 and Figure 7 indicates that the intersection of the advancing abutment pressure curve and the original rock stress curve is located at 8.1 m ahead of the working face. The boundary between the rapid deformation stage and the deceleration deformation stage of the roadway is 8.9 m in front of the working face and the distance between the stages is 0.8 m. The peak position of the advancing abutment pressure is at 19.8 m. The boundary between the deceleration deformation stage and the stable small deformation stage of the roadway is at 20.1 m and the distance between the stages is 0.3 m.

Based on the results of the theoretical analysis and the field measurement, we obtained the relationship between the advancing abutment pressure and the surrounding rock deformation stage of the roadway (Figure 8).

![Diagram](image)

**Fig. 8 Relationship between the advancing abutment pressure and the surrounding rock deformation of a roadway**

The results show that the boundary between the failure zone (rapid deformation stage) and the limit equilibrium zone (deceleration deformation stage) is the intersection of the advancing abutment pressure curve and the original rock stress line. The damaged area (rapid deformation phase) and the limit equilibrium area (slow deformation stage) constitute the plastic zone (large deformation stage). The boundary between the plastic zone (large deformation stage) and elastic zone (stable small deformation stage) is located at the peak value of the advancing abutment pressure.
5 Conclusions

A theoretical analysis and field measurements are used to analyze the relationship between the advancing abutment pressure and the surrounding rock deformation characteristics of the roadway of the j7401 fully-mechanized working face. The following conclusions are drawn:

We put forward a method of separating the surrounding rock deformation of the roadway in front of the working face into three stages: the rapid deformation stage, the deceleration deformation stage, and the stable small deformation stage. The rapid deformation stage and deceleration deformation stage occur in the plastic zone of the surrounding rock deformation and represent the large deformation stage. The stable small deformation stage occurs in the elastic zone of the surrounding rock deformation.

The relationship between the advancing abutment pressure and the deformation stage of the surrounding rock of the roadway is determined by integrating the results of the theoretical analysis and field measurements. The boundary between the failure zone (rapid deformation stage) and the limit equilibrium zone (deceleration deformation stage) is the intersection of the advancing abutment pressure curve and the original rock stress curve. The boundary between the plastic zone (large deformation stage) and the elastic zone (stable small deformation stage) is located at the peak value of the advancing abutment pressure.

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