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AHP AND TOPSIS BASED SELECTION OF ALUMINIUM ALLOY FOR AUTOMOBILE PANELS

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Abstract: Automotive industry is a very attractive area for young researchers to do continuous research and also it can be considered as an important thrust area as it is directly related to passenger safety. New developments in automotive sector can be seen in many domains like material selection, design, manufacturing etc. Since wrong selection directly leads to product failure, among these, the proper selection of a particular material can be treat as utmost priority. Hence, the present work discusses a methodology to select the best aluminium alloy for automobile panels among various alternates serving the same purpose. Analytical Hierarchy Process (AHP) and Technique for Order of Preference by Similarity to Ideal Solution (TOPSIS) methods with entropy weighting criteria are implemented for finding the best material and the results are discussed.

Keywords: Material selection, MADM methods, AHP, TOPSIS, aluminium alloys

1. INTRODUCTION

Automotive designers are seeking for lightweight materials with greater strengths. In modern vehicles, many automotive parts made of steel are being replaced with aluminium for weight reduction which enhances the fuel economy and consequently reduces the CO₂ emissions [1]. Excellent properties of aluminium alloy such as high strength, corrosion resistance and weldability drives young researchers to forward the research with aluminium as an alternate to steel.

Further, keeping weight reduction as main objective for most of the auto motor components previously generated by casting and extrusion are replaced by sheets parts as shown in Fig. 1.

The shape generated by steel sheet cannot be developed by aluminium alloys without failures because of its design shape limits and lower degree of freedom in forming. General failures such as wrinkling in steel are modified by improving the blank holder force which cannot be applied for aluminum alloys as it creates cracks leading to damage of components. Compared to steel, aluminum has 1/3 modulus of elasticity, low anisotropy values which tend to extensive local deformation. So the design of automotive panels with Aluminum alloys is always a challenging mission for the designers.

Fig. 1. Exploded view of Audi A8 space frame (a) and closures by weight (b)

However, a wide variety of aluminium alloys are available for a particular application. The selection of specific alloy by satisfying all the constraints without derailing the functional failure is always a major task.
So far the manufacturers used Trial and error method which is not valid every time. Multi Attribute Decision Making (MADM) methods are being more popular now a day to solve the critical situations of decision making in a systematic and logical way. These methods use simple mathematical formulae in complex decision making also. So far these methods are applied in many fields like Staff Selection [3], Alloy wheel material selection using magnesium alloys [4], Pharmacy product selection [5] and in many more [6].

Therefore, this paper exposes an organized approach for the selection of good material for automobile panels by the application of some MADM methods. Section 2 discuss the problem formulation while the section 3 and 4 describe the methodology and implementation of algorithms. Finally, conclusions are presented.

2. PROBLEM STATEMENT

As mentioned in the earlier section, the weight of an automobile can be reduced by replacing steel with an alternate material namely Aluminium. Cantor et al. [7] and Toroset al. [8] observed that depending on different regions and different manufacturing strategies wide range of aluminium alloys are applied in body panels. Based on features such as strength and formability, various alloys such as Heat treatable and non-heat treatable alloys are used in panels, developed from deep drawing process [9]. Further a survey is conducted on the available literature [10-13] w.r.t. Aluminium alloys and their necessary properties used in the automotive industry in view of panel applications. The researchers highlighted the prospects of various alloys that are being currently used as well as the research potentials of Al alloys in the near future. It is further observed that there are various alloys serving for the common application with each alloy is having its own merits and demerits. The alloys considered in the present study are tabulated in Table 1.

The problem is modelled to select the best alloy among ten different materials satisfying seven criterions. This problem is complex as the second material possesses’ good thermal conductivity while the first material has good percentage of elongation. 6061 with T6 condition i.e. material 10 is a good choice in view of good ultimate tensile strength and hardness. The material for panel application must be the fittest of all. Therefore, the problem is modelled to identify and to select the best alloy among the compared with MADM methods. The problem considered here is also a multi objective type as such it has to satisfy all the constraints and must produce a good quality solution.

3. METHODOLOGY

Multi Attribute Decision Making (MADM) methods or Multi Criterion Decision Making (MADM) methods are used when decision making is critical. These methods work with simple mathematical formulae and becoming more popular in the recent years in view of applications in vide fields. The generalised procedure of these MADM methods are depicted in Fig. 2.

There are a sub class of methods like SAW, WPM, AHP, TOPSIS, VIKOR, PROMETHEE, ELECTRE etc under the common name MADM or MCDM. Among these SAW and WPM methods are simple and AHP and TOPSIS are more popular in view of high potentiality in various fields [14, 15].

| S.No | Material | Density (g/cm³) | Thermal conductivity (W/mK) | Percentage of Elongation at break | Elastic modulus (GPa) | UTS (MPa) | YTS (MPa) | Hardness (BHN) |
|------|----------|----------------|-----------------------------|----------------------------------|----------------------|-----------|-----------|---------------|
| 1    | AA6016-T4 | 2.7            | 190                         | 27                               | 69                   | 200       | 110       | 55            |
| 2    | AA6016-T6 | 2.7            | 210                         | 11                               | 69                   | 280       | 210       | 80            |
| 3    | AA5182-O  | 2.65           | 130                         | 12                               | 68                   | 280       | 130       | 69            |
| 4    | AA5754-O  | 2.67           | 130                         | 19                               | 68                   | 210       | 90        | 52            |
| 5    | AA5454-O  | 2.69           | 130                         | 17                               | 69                   | 240       | 100       | 61            |
| 6    | AA5052    | 2.68           | 140                         | 22                               | 68                   | 190       | 79        | 47            |
| 7    | AA5454    | 2.69           | 130                         | 17                               | 69                   | 240       | 100       | 61            |
| 8    | AA5154    | 2.66           | 130                         | 20                               | 68                   | 240       | 94        | 58            |
| 9    | AA6061-T4 | 2.7            | 170                         | 18                               | 69                   | 230       | 130       | 63            |
| 10   | AA6061-T6 | 2.7            | 170                         | 10                               | 69                   | 310       | 270       | 93            |
3.1. AHP method
AHP stands for Analytical Hierarchy Process developed by T.L. Sathy in 1980. It is one of the most popular methods of MADM with many advantages. The major distinctive feature of the AHP method is to use pair-wise comparisons for comparing the alternatives with respect to the various criteria. It is easy to use and has a lot of interdependence of parameters for better output. The ability of to handle large size problems is another advantage of using this method [15, 16].

3.2. TOPSIS Method
Technique for Order of Preference by Similarity to Ideal Solution (TOPSIS) is another method under the category of MADM methods. In 1981, Ching-Lai Hwang and Yoon developed this method. This method is an approach to identify an alternative which is closest to the ideal solution and farthest to the negative ideal solution in a multi-objective environment. After the weights calculation and normalization of data, identify the positive alternatives in and calculate the separation measures of each alternate. Then evaluate the relative closeness and rank. The detailed formulae and examples in calculating performance is widely available in web [3, 5]. The advantage of this method is its ease in usage irrespective of problem size. TOPSIS has been successfully implemented in both Engineering, management, and business and marketing domains [15].

3.3. Entropy method
Entropy method uses the decision table to compute the weights regardless of operator’s choice. Entropy methods have gained much importance in the recent years as these methods reduce the decision makers experiments as much as possible by implementing mathematical computation for determining the weights. A detailed procedure of entropy method is given by Farhad Hosseinzadeh Lotfi et al. [17]. In entropy method, the higher the difference in performance values is considered for more weightage and the materials with similar performance was given with lower weightage.

Tab. 2. Normalized data of decision Table 1

| S.No | Material | Density (g/cm$^3$) | Thermal conductivity (W/mK) | Percentage of Elongation at break (%) | Elastic modulus (GPa) | UTS (MPa) | YTS (MPa) | Hardness (BHN) |
|------|----------|-------------------|-------------------------------|--------------------------------------|----------------------|----------|----------|---------------|
| 1    | AA6016-T4 | 0.98148           | 0.90476                       | 1.00000                              | 1.00000              | 0.64516  | 0.40741  | 0.59140       |
| 2    | AA6016-T6 | 0.98148           | 1.00000                       | 0.40741                              | 1.00000              | 0.90323  | 0.77778  | 0.86022       |
| 3    | AA5182-O  | 1.00000           | 0.61905                       | 0.44444                              | 0.98551              | 0.90323  | 0.48148  | 0.74194       |
| 4    | AA5754-O  | 0.99251           | 0.61905                       | 0.70370                              | 0.98551              | 0.67742  | 0.33333  | 0.55914       |
| 5    | AA5454-O  | 0.98513           | 0.61905                       | 0.62963                              | 1.00000              | 0.77419  | 0.37037  | 0.65591       |
| 6    | AA6052    | 0.98881           | 0.66667                       | 0.81481                              | 0.98551              | 0.61290  | 0.29259  | 0.50538       |
| 7    | AA5454    | 0.98513           | 0.61905                       | 0.62963                              | 1.00000              | 0.77419  | 0.37037  | 0.65591       |
| 8    | AA5154    | 0.99624           | 0.61905                       | 0.74074                              | 0.98551              | 0.77419  | 0.34815  | 0.62366       |
| 9    | AA6061-T4 | 0.98148           | 0.80952                       | 0.66667                              | 1.00000              | 0.74194  | 0.48148  | 0.67742       |
| 10   | AA6061-T6 | 0.98148           | 0.80952                       | 0.37037                              | 1.00000              | 1.00000  | 1.00000  | 1.00000       |
4. RESULTS AND DISCUSSIONS

The implementation of MADM methods uses a sequence of steps as mentioned in Section 3. After the preparation of decision table (Table 1), the next step is preparing the Normalized Table based on beneficiary and non-beneficiary variables. MATLAB software is implemented to generate the data from the equations. Normalized matrix for the problem considered is shown in Table 2.

The weights were computed according to Entropy method and are tabulated in Table 3. From Table 3, it can be observed that the large difference in YTS values of all the materials lead to higher weights while the weightage factors of density and Elastic modulus are very low. These values are corresponding to almost similar performance behavior of all materials in the decision table. It can also be understood that the selection of best material does not much influenced by these attributes.

4.1. AHP method

As per the procedure of AHP method, pair wise comparison of each alternate with other is prepared. Sample of pair wise matrices for alternatives 1, 10 are given in Table 4 (a) & (b).

After obtaining the pairwise comparison matrices, the overall performance of alternatives i.e materials is obtained by multiplying the relative weight of each criterion with its consequent weight value of each alternative and summing over the characteristic for each alternative. The performance scores of each material obtained from AHP are shown in Fig. 3.

| Density (g/cm²) | Thermal conductivity (W/mK) | Percentage of Elongation at break | Elastic modulus (GPa) | UTS (MPa) | YTS (MPa) | Hardness (BHN) |
|----------------|-----------------------------|----------------------------------|----------------------|-----------|-----------|----------------|
| 0.000121       | 0.094519                    | 0.241070                         | 0.000146             | 0.063899  | 0.48693   | 0.113311       |

Tab. 3. Entropy Weights for the attributes

| (a) Material 1 |
|----------------|
| 1 2 3 4 5 6 7 8 9 10 |
| 1 1.0000 1.0000 0.9818 0.9888 0.9963 0.9925 0.9963 0.9851 1.0000 1.0000 |
| 2 1.0000 1.0000 0.9818 0.9888 0.9963 0.9925 0.9963 0.9851 1.0000 1.0000 |
| 3 1.0188 1.0188 1.0000 1.0075 1.0150 1.0113 1.0150 1.0037 1.0188 1.0188 |
| 4 1.0112 1.0112 0.9925 1.0000 1.0074 1.0037 1.0074 0.9962 1.0112 1.0112 |
| 5 1.0037 1.0037 0.9851 0.9925 1.0000 0.9962 1.0000 0.9888 1.0037 1.0037 |
| 6 1.0074 1.0074 0.9888 0.9962 1.0037 1.0000 1.0037 0.9925 1.0074 1.0074 |
| 7 1.0037 1.0037 0.9854 0.9925 1.0000 0.9962 1.0000 0.9888 1.0037 1.0037 |
| 8 1.0150 1.0150 0.9962 1.0037 1.0112 1.0075 1.0112 1.0000 1.0150 1.0150 |
| 9 1.0000 1.0000 0.9814 0.9888 0.9963 0.9925 0.9963 0.9851 1.0000 1.0000 |
| 10 1.0000 1.0000 0.9814 0.9888 0.9963 0.9925 0.9963 0.9851 1.0000 1.0000 |

| (b) Material 10 |
|----------------|
| 1 2 3 4 5 6 7 8 9 10 |
| 1 1.0000 0.6875 0.7971 1.0576 0.9016 1.1702 0.9016 0.9482 0.8730 0.5914 |
| 2 1.4545 1.0000 1.1594 1.5384 1.3111 1.7021 1.3111 1.3793 1.2698 0.8602 |
| 3 1.2545 0.8625 1.0000 1.3269 1.1311 1.4680 1.1311 1.1896 1.0952 0.7419 |
| 4 0.9454 0.6500 0.7536 1.0000 0.8524 1.1063 0.8524 0.8966 0.8254 0.5591 |
| 5 1.1090 0.7625 0.8840 1.1730 1.0000 1.2978 1.0000 1.0517 0.9682 0.6559 |
| 6 0.8545 0.5875 0.6811 0.9038 0.7704 1.0000 0.7704 0.8103 0.7460 0.5053 |
| 7 1.1090 0.7625 0.8840 1.1730 1.0000 1.2978 1.0000 1.0517 0.9682 0.6559 |
| 8 1.0545 0.7250 0.8405 1.1153 0.9508 1.2340 0.9508 1.0000 0.9206 0.6236 |
| 9 1.1454 0.7875 0.9130 1.2115 1.0327 1.3404 1.0327 1.0862 1.0000 0.6774 |
| 10 1.6909 1.1625 1.3478 1.7884 1.5245 1.9787 1.5245 1.6034 1.4761 1.0000 |

Tab. 4. Pair Wise comparison matrices for each material
It can be seen from Fig. 3 that the highest performance score is for AA6061 – T6 material and the order of preference for the selection of materials according to AHP is 10 - 2 - 1 - 9 - 3 - 8 - 7 - 5 - 4 - 6.

4.2. TOPSIS method

With the normalized matrix and Weight matrix, Normal Decision matrix $R_{ij}$ and Weighted Normalized matrix $V_{ij}$ are computed. From weighted normalized matrix, the ideal best and worst solutions ($V^+$, $V^-$) as well as the separation measures ($S^+$, $S^-$) for each alternate is calculated with the TOPSIS formulae are shown below in Table 5 and 6.

### Table 5. Ideal Best and Ideal Worst Solutions ($V^+$, $V^-$)

| Attributes | $V^+$ | $V^-$ |
|------------|-------|-------|
| 1          | 0.00003 | 0.00003 |
| 2          | 0.04034 | 0.02497 |
| 3          | 0.11433 | 0.04234 |
| 4          | 0.00004 | 0.00004 |
| 5          | 0.02599 | 0.01568 |
| 6          | 0.28961 | 0.08473 |
| 7          | 0.05110 | 0.02582 |

### Table 6. Separation measures of materials ($S^+$, $S^-$)

| Materials | $S^+$ | $S^-$ |
|-----------|-------|-------|
| 1         | 0.1731 | 0.0802 |
| 2         | 0.0937 | 0.1427 |
| 3         | 0.1643 | 0.0571 |
| 4         | 0.1980 | 0.0400 |
| 5         | 0.1887 | 0.0382 |
| 6         | 0.2081 | 0.0508 |
| 7         | 0.1887 | 0.0382 |
| 8         | 0.1927 | 0.0458 |
| 9         | 0.1561 | 0.0654 |
| 10        | 0.0723 | 0.2068 |

By using the data of Table 6. The performance scores of each material is calculated and is shown in Fig. 4.

As seen from Fig. 4, AA 6061 – T6 has the highest performance score than the other materials and the order of preference for the selection of materials in panel application according to TOPSIS is 10 - 2 - 1 - 9 - 3 - 6 - 8 - 7 - 5 - 4.
4.3. Comparison of both methods

Based on the performance scores obtained from AHP and TOPSIS, Ranking was given to each material and tabulated in Table 7.

| S.No | Material | AHP RANK | TOPSIS RANK |
|------|----------|----------|-------------|
| 1    | AA6016-T4 | 3        | 3           |
| 2    | AA6016-T6 | 2        | 2           |
| 3    | AA5182-O  | 5        | 5           |
| 4    | AA5754-O  | 9        | 10          |
| 5    | AA5454-O  | 8        | 9           |
| 6    | AA5052    | 10       | 6           |
| 7    | AA5454    | 7        | 8           |
| 8    | AA5154    | 6        | 7           |
| 9    | AA 6061-T4| 4        | 4           |
| 10   | AA6061-T6 | 1        | 1           |

It can be observed that, the ranking of materials is not uniform as each method has its own procedure to rank the alternates. However, for this particular problem both methods suggested AA 6061-T6 is the best choice of material. So the usage of AA 6061 – T6 material will enhance the performance of automobile panel as suggested by MADM methods.

5. CONCLUSIONS

In view of weight reduction strategies in automotive industry, the replacement of steel with aluminium is found to be the best option. As there are number of Aluminium alloys for the same purpose and to replace with the suitable alloy satisfying the functional requirement is a challenging task. Ten different alloys with seven attributes are considered in the present study. The procedure involved for the selection panel applications by the class of MADM methods like AHP and TOPSIS is given in detail and are successfully implemented. Entropy method was adopted to find the weights and are incorporated to find the solution quality. From the results, it is observed that the material AA6061 with T6 condition is the best alternate. Though the two methods AHP and TOPSIS differ in the respective procedures but for this particular problem the both methods suggested the same material as the best choice. The present approach tries to find the best material in a logical way, still further research should be carried out for practical application of the proposed material in the respective field.

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Nomenclature

The following Nomenclature is used in the present study

| Symbols | Description |
|---------|-------------|
| V⁺, V⁻ | Ideal Best and Worst Solutions |
| S⁺, S⁻ | Separation Measures |
| T4     | Solution heat treated with natural aging |
| T6     | Solution heat treated with Artificial aging |
| O      | Annealed |

| Acronyms | Meaning |
|----------|---------|
| MADM     | Multi Attribute Decision Making |
| AHP      | Analytical Hierarchy Process |
| TOPSIS   | Technique for Order of Preference by Similarity to Ideal Solution |
| SAW      | Simple Additive Method |
| WPM      | Weighted Product Method |
| VIKOR    | Vlse Kriterijumska Optimizacija Kompromisno Resenje (Vilks Kriterium Optimization Compromise Solution) |
| PROMETHEE| Preference ranking organization method for enrichment evaluation |
| ELECTRE | ELimination and Choice Expressing REality |
| BHN      | Brinell Hardness Number |
| UTS      | Ultimate Tensile Strength |
| YTS      | Yield Tensile Strength |
| AA       | Aluminium Alloy |

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