Digital image correlation for sensing kinematic fields in manufacturing processes: a review

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Abstract

Purpose – The purpose of the work is to provide a comprehensive review of the digital image correlation (DIC) technique for those who are interested in performing the DIC technique in the area of manufacturing.

Design/methodology/approach – No methodology was used because the paper is a review article.

Findings – No findings.

Originality/value – Herein, the historical development, main strengths and measurement setup of DIC are introduced. Subsequently, the basic principles of the DIC technique are outlined in detail. The analysis of measurement accuracy associated with experimental factors and correlation algorithms is discussed and some useful recommendations for reducing measurement errors are also offered. Then, the utilization of DIC in different manufacturing fields (e.g. cutting, welding, forming and additive manufacturing) is summarized. Finally, the current challenges and prospects of DIC in intelligent manufacturing are discussed.

Keywords Digital image correlation, Kinematic fields, Manufacturing process, Sensing

1. Introduction

For decades, more and more attention is being paid to intelligent manufacturing with the capability of manufacturing various products with minimal supervision and assistance from operators (Zhou et al., 2018). Vigorously developing intelligent manufacturing is of great significance for improving production efficiency, intelligentization and green growth of manufacturing. However, the realization of intelligent manufacturing still faces many challenging issues. As one of the core issues in intelligent manufacturing, measurement technology is an essential part that provides intelligent perception, which is the basis of detection, control and decision in the whole manufacturing process. So far, in-depth works have been done for developing measurement technology in the manufacturing field by many researchers, and a variety of innovative methods have been explored, mainly focusing on the measurement of kinematic fields to obtain displacement and strain information, such as mechanical tests (fatigue, fracture, impact, etc.) and materials processing (welding, forming, cutting, etc.). Several commonly employed methods for the displacement or deformation measurement could be categorized as (1) the finite difference of the rigid-body displacement at the edge of the observed structure (Harangus and Kakucs, 2014) and (2) glued strain gages (Little, 1992; Zhang, 2019).
In the first scenario, the desired displacement measurements are obtained by the relative motion of the two arms of the extensometer, either on the tester itself or glued or clamped to a specific point on the surface. Except from the practical issues of realization, the information acquired should be averaged between the points where the motion is known. Since the local phenomena are negligible, the position and size of the detection would be unknown. In the second case, it is clear that the utilization of strain gages is a contact measurement with the following several inherent limitations. (1) For small specimens or soft materials, the additional stiffness and weight of the strain gauges can seriously affect the measurement results, since the gages are glued to the surface of the specimen during the measurement. (2) Strain gages as a point measurement method cannot obtain full-field information and are not applicable to the measurement of non-uniform deformation. (3) The limited measurement range of strain gages means that the resistive wire of strain gages will fail when measuring large deformations (Zhang, 2019). In contrast, optical measurements, as a non-contact full-field measurement method, can handle the above mentioned issues. Many optical measurement methods allow quantization of displacement, including (1) interferometric techniques such as holographic interferometry (Georges, 2019), speckle scattering interferometry (Asseban et al., 2000) and moiré interferometry (Walker, 1994) and (2) non-interferometric techniques such as DIC and particle image velocimetry (PIV) (Grant, 1997).

Usually, deformation is obtained by interpreting the interference in interferometric optical measurements. More concretely, interferometry is achieved by projecting a specific pattern (grid, line or speckle) onto the exact same pattern that is painted on the object to be imaged. The superposition discrepancy represents mainly local displacements and produces an image where the deconstructed displacements can be quantified. In addition, laser interferometry is performed by recording the phase change of scattered light waves from the surface of the object under test. Given the high-speed scanning, laser interferometry can be applied to point measurements or in situ measurements. The technique usually requires a coherent light source, i.e. a laser. However, it is critical to meet environmental requirements when performing interferometric measurements, which are usually performed in vibration-isolated optical platforms. Therefore, these techniques are commonly used in laboratories and are difficult to apply in industrial applications due to the complexity of the environment. For non-interferometric optical measurements, only a non-coherent light source is necessary to acquire the deformation of the surface by comparing the grayscale intensity changes; thus, they are more accessible than interferometric optical measurement methods (Zhang, 2019). The DIC method is a representative non-interferometric measurement method that has been extensively used to measure the deformation of solid materials. A typical workflow of DIC displacement measurement is shown in Figure 1 (Hild and Roux, 2006; Pan et al., 2009, 2018; Schreier et al., 2009; Dong and Pan, 2017; Pan, 2018). In general, for the manufacturing field, the DIC technique is a promising optical method that can overcome most of the above limitations. In addition, the PIV technique is commonly used for flow-field analysis.

This work is intended to provide a comprehensive review of the DIC technique for those who are interested in performing the DIC technique in the area of manufacturing. A historical overview of DIC is introduced in Section 2. Section 3 elaborates on the main advantages of DIC. The measurement setup and basic principles of DIC are outlined in Section 4 and 5, respectively. The influencing factors on the measurement accuracy of DIC are discussed in Section 6 and some recommendations for reducing measurement errors are correspondingly offered. Section 7 focuses on the applications of DIC in different manufacturing fields. At the end of this review, the persistent challenges and future direction of DIC for intelligent manufacturing are discussed.
2. Historical overview of DIC

In the early 1980s, the idea of the DIC technique was first proposed by Yamaguchi (1981a, b) and Bruck et al. (1989). Yamaguchi studied the deformation of small objects by calculating the correlation function of the intensity of speckle illumination. A few years later, Peters and Ranson adopted iterative operations for digital images of objects acquired from before and after deformation. They derived the extreme values of the correlation coefficients by calculating the correlation coefficients and their derivatives with displacement to obtain the corresponding displacements. Many researchers have done intensive work on how to fasten the speed and improve the accuracy of the calculation. Peters et al. applied the DIC technique for the first time to measure the displacement of a stiff body (Peters et al., 1983). Sutton et al. improved the correlation search methodology and used a combination of coarse and fine correlation to enhance the computational speed (Sutton et al., 1983). HE et al. investigated the accuracy of the DIC technique and improved the theory of this measurement method (He et al., 1984). Sutton et al. analyzed the measurement error arising from the sub-pixel recovery process and proposed reasonable methods for dealing with sub-pixel recovery (Sutton et al., 1986). Bruck et al. adopted the Newton–Raphson (NR) iterative algorithm based on binary cubic-spline interpolation sub-pixel reconstruction to solve the DIC problem, which significantly improved the DIC method (Bruck et al., 1989). Vendroux and Knauss used the first-order derivative approximation for the Hessian matrix, replacing the NR algorithm with the Gauss–Newton algorithm, which improved the computational efficiency by eliminating the process of calculating the second-order gray gradient while ensuring the computational accuracy (Vendroux et al., 1998; Vendroux and Knauss, 1998; Vendroux et al., 1998).

Since 2000, DIC technology has entered a boom period with the continuous development of computer technology and the increasing accessibility of imaging devices (Pan, 2018).
Research in this phase has focused on (1) new imaging systems (Schreier et al., 2004; Berfield et al., 2006; Louis et al., 2007) and the characterization and correction of device-induced measurement errors (Jin and Bruck, 2005; Luo, 2006); (2) speckle pattern fabrication and quality evaluation (Reu, 2014; Lecompte et al., 2006; Stoilov et al., 2012; Zhang et al., 2018); (3) development of correlation algorithm (Tong, 2005; Pan, 2009) and (4) evaluation of DIC measurement errors (Lecompte et al., 2006; Haddadi and Belhabib, 2008; Sutton et al., 2008; Bornert et al., 2009; Wang et al., 2009). For instance, Peng et al. used a computer to generate digital images with random speckles according to Gaussian intensity distribution in order to simulate the displacement speckle pattern of the object before and after deformation in 2001 (Zhou, 2001). In this work, an iterative, spatial-gradient-based algorithm was developed that requires the calculation of only first-order spatial derivatives of the images and thus reduces the computation complexity. In 2006, Pan et al. conducted a detailed and systematic study and evaluation of the systematic errors and random errors of the existing sub-pixel displacement measurement algorithms in which a conclusion that the NR algorithm based on spatial iterative cross-correlation (CC) is more accurate but much slower than other algorithms (Pan et al., 2006). Later, Pan et al. made a detailed analysis of the selection of subset size and quantitative evaluation of speckle quality, and also mathematically derived the theoretical model of displacement measurement accuracy of the two-dimensional DIC method (Pan et al., 2008). More recently, Shao et al. proposed a pixel-selection strategy to improve the computational efficiency of DIC further, which allows a real-time deformation measurement with a large subset (Shao et al., 2020).

Many essential advances have been made, making DIC one of the most popular and practical measurement techniques. Meanwhile, over the years, the DIC technique has been extended from the initial displacement analysis in metal detection to many other fields such as biomechanics (Palanca et al., 2016), civil engineering (Ramos et al., 2015), aerospace (Chu and Poudel, 2014), electronics (Niu et al., 2018) and so on. In addition, with the advent of atomic force microscopy, transmission electron microscopy and scanning tunneling microscopy, DIC is widely used for microscopic observation (Budyn et al., 2012). Specifically, these applications are concentrated in the areas (Zhang, 2019) as follows:

1. Measure deformation properties and mechanical properties of diverse materials (e.g. metals, composites, polymers and wood) under mechanical and thermal loads. Zink et al. first used the DIC technique to study the mechanical properties of wood (Audrey and Robert, 1983). Choi et al. applied the DIC technique to measure the deformation of concrete under compressive loading and to obtain the failure performance of concrete (Choi and Shah, 1997). Bastawros et al. applied the DIC technique to obtain three stages of the deformation process of the aluminum alloy foam under compressive loading (Bastawros et al., 2000). Chevalier et al. studied the axial tensile tests of a kind of polymer by DIC (Chevalier et al., 2001).

2. From displacement and strain information acquired by the DIC technique, various material parameters such as modulus of elasticity, Poisson’s ratio, coefficient of thermal expansion, stress intensity factor, fracture toughness, etc. can be evaluated. For instance, Zhang et al. studied the variation of Poisson’s ratio of the arterial vessels with axial strain by DIC (Zhang et al., 2002). Yoneyama (2006) and Réthoré et al. (2005) adopted the DIC technique to measure the stress intensity factor at the crack tip.

3. The full-field deformation data of the object surface obtained by the DIC technique are utilized for theoretical analysis and numerical simulations (Knauss et al., 2003; Cho et al., 2005; Sabaté et al., 2006). Thus, theory, simulation and experiment can be well linked to achieve in-depth and thorough analysis.
3. Advantages of DIC technique
The emergence and development of DIC were made possible by the rapid development of camera technology and the computing power of personal computers. The DIC method has a number of attractive advantages over other traditional measurement techniques as follows (Zhang, 2019):

Simple experimental setup: The main device has only one camera, such as a charge-coupled device (CCD) or a complementary metal-oxide-semiconductor (CMOS), which is intended to record images of the surface of an object during its movement.

Simple specimen preparation: If the surface of the specimen has a natural texture with random gray intensity distribution, the specimen can be used directly, where the natural texture can be considered as speckles for easy tracking in the DIC. If not, the sample surface can be easily prepared by spraying black and/or white paint as speckles.

Strong environmental adaptability: The DIC technique does not require a laser source; typically, a white light source or natural light is sufficient for the measurement. Preferably, the illumination of the imaging scene remains constant throughout the recording process, while relatively small variations in illumination can also be tolerated as long as the surface texture is unique. In addition, DIC can be applied to complex operating conditions such as high temperature, high pressure, high-speed impact, vibration, etc. Therefore, DIC technology is well suited for industrial applications such as manufacturing processes.

Wide measurement range: The DIC method is expected to directly process digital images that can be acquired with various high-resolution digital acquisition devices, such as optical microscopes (Sun et al., 1997; Pitter et al., 2002), laser scanning confocal microscope (Berfield et al., 2006; Franck et al., 2007), scanning electron microscopy (Kang et al., 2005; Wang et al., 2006), transmission electron microscopy (Calvié et al., 2014), atomic force microscopy (Chang et al., 2005; Sun and Pang, 2006), scanning tunneling microscope (Vend and Knauss, 1998; Vendroux and Knauss, 1998; Vendroux et al., 1998) and satellites (Leprince et al., 2007). All these types of images can be analyzed by the DIC method, which makes it possible to measure displacements from microscopic to macroscopic scales using the DIC method.

4. DIC measurement setup
4.1 Specimen preparation
Surface patterns on the test specimen are essential for DIC, i.e. there must be sufficiently recognizable patterns on the surface of the measured object. As a carrier of displacement information, the surface pattern should possess the features of high contrast, randomness, isotropy and stability in order to achieve accurate DIC measurements (Dong and Pan, 2017). Except for a few specimens with natural texture on their surfaces, such as the grains on the metal surface or milling streaks, artificial speckles made by spraying black and/or white paints are required. Spray painting is currently the most common way to obtain speckle pattern, but manual spray is hard to control the quality of speckle. Some examples of speckles are schematically shown in Figure 2. Isotropic patterns ensure that displacements can be identified in each direction of the plane. The high-contrast speckle pattern makes sure that there is maximum gradient. An illustration of the best pattern is shown in Figure 2(d). The other three patterns are not good for performing DIC. In addition to spray painting, printing a speckle pattern is another way to firmly attach the printed speckle sticker to the specimen surface and deform it with the specimen. Nevertheless, if the printed speckle slips against the specimen surface due to creases and bubbles, the experimental data obtained from the image no longer reflect the actual deformation of the specimen (Zhang, 2019).

4.2 Image acquisition system
For a typical DIC image acquisition system, as shown in Figure 3, there are four main elements as follows: (1) a surface speckled specimen; (2) a silicon-based camera (CCD or
CMOS); (3) a computer for data acquisition and (4) a white light source. More specifically, the camera is placed on a tripod so that its optical axis is perpendicular to the sample surface. The white light source is intended to provide a good view of the surface of the specimen with a high-contrast grayscale intensity distribution. When the specimen is loaded, the camera records images of the specimen during the deformation process. The acquired images are
then processed \textit{a posteriori} by a computer to obtain the displacement field. In addition, the
strain field can be inferred from the displacement field (Zhang, 2019).

5. Basic principles of DIC
The fundamental principle of DIC method is to choose a reference subset with
\((2k + 1) \times (2k + 1)\) pixels \((k, \text{the number of pixels})\) in the reference image \(f(x, y)\), i.e. the
image acquired before deformation, and then to determine the corresponding subset location
in the deformed image \(g(x', y')\) based on the gray level information of the subset. It can be
noted that this justifies why the surface pattern cannot be repeated, otherwise the determined
solution may not be unique. Therefore, the displacement and strain can be obtained based on
the changes in the position and shape of a subset of the two images (Zhang, 2019).

To achieve the above goal, a correlation calculation is required in DIC. First, a suitable set
of variables should be found to represent the displacement and deformation of subsets in the
reference image and the deformation image. Second, a mathematical criterion should be
established to evaluate the degree of correspondence between the two subsets: one in the
reference image and the other in the final strain and displacement image. Finally, the
displacements and strains of the subsets are obtained by iterative calculations using an
efficient search algorithm.

5.1 Shape functions
As shown in Figure 4, a point \(P(x_0, y_0)\) is in the reference image. To calculate the displacement
of point \(P\), a reference subset centered on point \(P(x_0, y_0)\) of the reference image is utilized to
track its corresponding position in the deformed image. The reason for choosing a square
subset instead of individual pixels for matching is that the subset containing a wider range of
grayscale variations will be distinguished from other subsets and can, therefore, be identified
more uniquely in the distorted image (Zhang, 2019).

The subset centered at point \(P(x_0, y_0)\) moves to a location near point \(P'(x'_0, y'_0)\). The
displacement of point \(P\) on the \(x\) and \(y\) axes is \(u\) and \(v\), respectively. Thus,
\[
\begin{align*}
  x'_0 &= x_0 + u \\
  y'_0 &= y_0 + v
\end{align*}
\]  

Meanwhile, the point \(Q(x_i, y_i)\) represents any point around the point \(P\) in the reference subset;
the positional relationship between point \(P\) and point \(Q\) is given as follows:

![Figure 4. Schematically illustration of a reference square subset before deformation and a targeted subset after deformation](image-url)
\[ x_i = x_0 + \Delta x \]
\[ y_i = y_0 + \Delta y \] (2)

where \( \Delta x \) and \( \Delta y \) is the distance between point \( P \) and point \( Q \) on the \( x \) and \( y \) axes, respectively. If the point \( Q \) in the reference subset moves to point \( Q'(x'_i, y'_i) \), an equation can be given as follows:

\[ \begin{align*}
   x'_i &= x_i + u_Q \\
   y'_i &= y_i + v_Q
\end{align*} \] (3)

Generally, the material imaged in the reference subset allows translation, rotation and shear. Thus, the displacement of point \( Q \) on the \( x \) and \( y \) axes \((u_Q, v_Q)\) can be given by the first-order displacement gradient of point \( P \):

\[ \begin{align*}
   u_Q &= u + \frac{\partial u}{\partial x} \Delta x + \frac{\partial u}{\partial y} \Delta y \\
   v_Q &= v + \frac{\partial v}{\partial x} \Delta x + \frac{\partial v}{\partial y} \Delta y
\end{align*} \] (4)

Substituting Eq. (4) into Eq. (3) yield:

\[ \begin{align*}
   x'_i &= x_i + u + \frac{\partial u}{\partial x} \Delta x + \frac{\partial u}{\partial y} \Delta y \\
   y'_i &= y_i + v + \frac{\partial v}{\partial x} \Delta x + \frac{\partial v}{\partial y} \Delta y
\end{align*} \] (5)

Since point \( Q \) is any point in the subset, it is found from Eq. (5) that displacement of the subset can be expressed by the displacement of the center point in the subset and its four derivatives \((u, v, \frac{\partial u}{\partial x}, \frac{\partial u}{\partial y}, \frac{\partial v}{\partial x}, \frac{\partial v}{\partial y})\).

### 5.2 Correlation criterion

In order to assess the degree of similarity between the reference and deformation subsets, a correlation criterion should be given. Different correlation criteria have been proposed so far. Usually, the correlation criteria consist of two groups: CC criteria and the sum of squared differences (SSD) criteria. Three commonly used CC criteria are as follows (Zhang, 2019):

1. **Cross-correlation (CC):**
   \[ C_{CC} = \sum_{-k}^{k} \sum_{-k}^{k} [f(x, y) \cdot g(x', y')] \] (6)

2. **Normalized cross-correlation (NCC):**
   \[ C_{NCC} = \frac{\sum_{-k}^{k} \sum_{-k}^{k} [f(x, y) \cdot g(x', y')]}{\left[ \sum_{-k}^{k} \sum_{-k}^{k} f^2(x, y) \right]^{\frac{1}{2}} \cdot \left[ \sum_{-k}^{k} \sum_{-k}^{k} g^2(x', y') \right]^{\frac{1}{2}}} \] (7)
(3) Zero-normalized cross-correction (NCC):

\[
Z_{\text{NCC}} = \left\{ \sum_{k=-h}^{h} \sum_{-k}^{k} \left[ \frac{f(x, y) - f_m}{\sqrt{\sigma^2_f}} \right] \cdot \left[ \frac{g(x', y') - g_m}{\sqrt{\sigma^2_g}} \right] \right\} \]

where \( f_m = \frac{1}{(2k+1)^2} \sum_{-k}^{k} f(x, y) \) and \( g_m = \frac{1}{(2k+1)^2} \sum_{-k}^{k} g(x', y') \).

Three commonly used SSD criteria are given as follows:

1. Sum of squared differences (SSD):

\[
C_{\text{SSD}} = \sum_{k=-h}^{h} \sum_{-k}^{k} (f(x, y) - g(x', y'))^2
\]

2. Normalized sum of squared differences (NSSD):

\[
C_{\text{NSSD}} = \sum_{k=-h}^{h} \sum_{-k}^{k} \left[ \frac{f(x, y)}{\sigma_f} \right]^2 - \left( \frac{g(x', y')}{\sigma_g} \right)^2
\]

3. Zero-normalized sum of squared differences (ZNSSD):

\[
C_{\text{ZNSSD}} = \sum_{k=-h}^{h} \sum_{-k}^{k} \left[ \frac{f(x, y) - f_m}{\sqrt{\sigma^2_f}} \right] \cdot \left[ \frac{g(x', y') - g_m}{\sqrt{\sigma^2_g}} \right]
\]

The basic principles of these correlation criteria are the same. Here, the normalized CC (NCC) is used to be analyzed as an example. The definition of NCC is given as follows:

\[
C(x, y, u, v, \frac{\partial u}{\partial x}, \frac{\partial u}{\partial y}, \frac{\partial v}{\partial x}, \frac{\partial v}{\partial y}) = \sum_{k=-h}^{h} \sum_{-k}^{k} \left[ f(x, y) \cdot g(x', y') \right] \cdot \left[ \frac{\sum_{k=-h}^{h} \sum_{-k}^{k} f^2(x, y)}{\sqrt{\sum_{k} \sum_{-k} f^2(x, y)}} \right] \cdot \left[ \frac{\sum_{k=-h}^{h} \sum_{-k}^{k} g^2(x', y')}{\sqrt{\sum_{k} \sum_{-k} g^2(x', y')}} \right]
\]

where \( x, y \) are the coordinates of the center point in the subset and \( x', y' \) are the coordinates of any point in the subset and can be obtained by Eq. (5). When the maximum value is achieved (i.e. \( C = 1 \)), the subset in the deformed image is correlated with the reference subset in the reference image.

In correlation calculation, an optimization algorithm is normally adopted to find the minimum value. Thus, a correlation factor S is introduced as follows:
It is clear from Eq. (13) that the smaller the \( S \) value, the greater the correlation between the two subsets. Also, it is worth to note that the correlation values calculated by the ZNCC or ZNSSD criterion are changeless if only an offset and a scale in lighting, i.e. linear transformation of the target subset gray intensity. Thus, the ZNCC or ZNSSD criterion could accommodate changes in lighting. Meanwhile, the NCC or SSD correlation criterion is insensitive to the linear scale in lighting but sensitive to offset of the lighting. The CC or SSD correlation criterion is sensitive to all changes in lighting, as shown in Table 1.

5.3 Search algorithm

A vector \( J \) is introduced to represent the displacement of the subset, which is given as follows:

\[
J = \left\{ x, y, u, v, \frac{\partial u}{\partial x}, \frac{\partial u}{\partial y}, \frac{\partial v}{\partial x}, \frac{\partial v}{\partial y} \right\}
\]

\( J_i \) (\( i = 1, 2, 3, 4, 5, 6 \)) is utilized to represent the \( u, v, \frac{\partial u}{\partial x}, \frac{\partial u}{\partial y}, \frac{\partial v}{\partial x}, \frac{\partial v}{\partial y} \). Therefore, the correlation calculation is used to find the minimum of the objective function \( S(J_1, J_2, J_3, J_4, J_5, J_6) \). Obviously, the necessary condition for \( S \) to reach its minimum value is that its first-order derivative is zero.

| Name   | Formula                                                                 | Intensity changes |
|--------|-------------------------------------------------------------------------|-------------------|
| SSD    | \( \sum_{-k}^{k} \sum_{-k}^{k} |f(x, y) - g(x', y')|^2 \) | None              |
| NSSD   | \( \left( \sum_{-k}^{k} \sum_{-k}^{k} f(x, y) \right)^5 \left( \sum_{-k}^{k} \sum_{-k}^{k} g(x', y') \right)^5 \) | Scale             |
| ZNSSD  | \( \left( \sum_{-k}^{k} \sum_{-k}^{k} f(x, y) \right)^5 \left( \sum_{-k}^{k} \sum_{-k}^{k} g(x', y') \right)^5 \) | Scale + offset    |
| CC     | \( \sum_{-k}^{k} \sum_{-k}^{k} f(x, y) \cdot g(x', y') \) | None              |
| NCC    | \( \left( \sum_{-k}^{k} \sum_{-k}^{k} f(x, y) \right)^5 \left( \sum_{-k}^{k} \sum_{-k}^{k} g(x', y') \right)^5 \) | Scale             |
| ZNCC   | \( \left( \sum_{-k}^{k} \sum_{-k}^{k} f(x, y) \right)^5 \left( \sum_{-k}^{k} \sum_{-k}^{k} g(x', y') \right)^5 \) | Scale + offset    |

Table 1.
Summary of the common optimization criterion
For this optimization issue, there are many numerical methods such as NR, etc. When the $S$ reaches a minimum, we can obtain the displacement and deformation of the subset from the $J_i$ values (Zhang, 2019).

The process described above is the basic principle of the local image correlation method in which a small region of interest, i.e. the aforementioned reference subset, is selected for processing as shown in Figure 4. The main drawback of the approach is that the process could cause large fluctuations (from speckle and the variation of lighting) from one image to the other.

The main limitation of the local method is that the process can induce large fluctuations from one image to the other (from speckle and the variation of lighting). The global image correlation method is superior to the local method and avoids the limitations of the local method described above (Hild and Roux, 2012). The global method relies on the entire image to determine the displacement field based on mesh and shape functions (Besnard et al., 2006).

6. Errors affecting DIC measurements

Obviously, the estimation of the errors caused by different error sources is important to improve the measurement accuracy of DIC. DIC techniques rely on a complex measurement chain, so the measurement errors could stem from each of its elements. Generally, the cause of the measurement errors could be categorized into two parts: one is related to the correlation principle itself and the other is associated with the measurement devices and the working environment. In this section, different sources of measurement error are analyzed in detail and recommendations for avoiding these measurement errors are also offered.

Specifically, the errors related to the correlation principle itself could stem from (1) the quality of the speckle pattern, (2) the step size and the subset size and (3) the correlation algorithm. First, the speckle pattern on the specimen surface is the carrier of the deformation information of the specimen. The DIC collects the deformation information of the specimen by identifying and tracking the speckle field on the surface of the specimen. Thus, the quality of the speckle pattern is closely related to the measurement accuracy of DIC methods. The traditional evaluation parameters of speckle quality focus on reducing random errors, so fine speckle is normally used in experiments. However, speckle that is too fine will increase the interpolation deviation, which results in unsatisfactory experimental results. Researchers have tried to theoretically deduce the error related to the quality of the speckle pattern in DIC and the various evaluation mechanisms of the quality of the speckle pattern are given by them, such as mean speckle size (Lecompte et al., 2006), subset entropy (Yaofeng and Pang, 2007) and the sum of the square of subset intensity gradients (Pan et al., 2008) etc. As mentioned before, the creation of a surface pattern with the features of high contrast, randomness, isotropy and stability is essential to improve measurement accuracy.

Additionally, as a user-defined input parameter, the chosen step and subset size are also critical to the measurement accuracy. In order to achieve a reliable analysis of correlation, the subset size should be big enough so that there is a sufficiently distinctive intensity pattern included in the subset to distinguish itself from other subsets. Meanwhile, larger subsets require more computation time. On the other hand, whereas, the underlying deformation field of a small subset could be accurately approximated by the first- or second-order subset shape function, but a large subset size tends to lead to large errors in the approximation of the underlying deformations. Therefore, the chosen subset size should be small so as to
guarantee reliable results of displacement measurement. Based on the aforementioned two conflicting requirements, there should be a trade-off in the choice of subset size (Pan et al., 2009). Besides, the step size has a stronger effect on spatial resolution than the subset size, i.e. smaller step sizes yield more DIC data points and thus higher spatial resolution.

In addition, the correlation algorithm affects the measurement accuracy of DIC methods, influencing factors including shape function, interpolation scheme, correlation criterion, etc. When the subset size is small, the first-order shape function or the second-order shape function could accurately describe the displacement of the points in the subset. However, they are obtained by expending the displacement function of points in the subset at the center of the subset using the first-order or second-order Taylor series expansion, which are an approximation of actual values. Scherier et al. analyzed the systematic errors introduced by the shape function in the DIC method (Schreier and Sutton, 2002). They concluded that although the second-order shape function cannot improve the calculation accuracy of the displacement derivative, it could reduce the systematic error introduced by the shape function. And in some cases, the second-order shape function could describe the deformation more accurately than the first-order shape function. Besides, measurement error could also be introduced by the use of interpolation schemes. In the DIC, so far, a variety of interpolation algorithms have been utilized to perform the grayscale reconstruction of sub-pixel, including bilinear interpolation (Bruck et al., 1989), bicubic interpolation (Jin, 2005) etc. However, sub-pixel interpolation could only approximately restore the grayscale of the image and cannot acquire the completely correct value of grayscale. Schreier et al. investigated the impact of interpolation phase error on the matching error in DIC and high-order interpolation methods with smaller phase errors are recommended to reduce these systematic errors (Schreier, 2000). Additionally, the correlation criterion also has an effect on the measurement accuracy due to the variation in grayscale in the actual environment, such as changes in lighting. As mentioned before, the ZNCC or ZNSSD criterion could accommodate changes in lighting and thus are recommended in the correlation criterion.

On the other hand, the measurement errors caused by the measurement devices and the working environment cannot be despised either. First of all, the DIC method obtains the surface image of the specimen through the optical lens, whereas the common optical lens inevitably has image distortion. Therefore, it is helpful to estimate the distortion of the camera lens for improving the measurement accuracy. The correction of lens distortion could be divided into two categories: one is that correcting the distortion by solving the distortion coefficient of the known distortion model (Yoneyama, 2006) and the other type is based on camera calibration (Helm, 1996), which is characterized by other parameters of the camera being solved together. Notably, the former method is mostly used for two-dimensional DIC, while the latter method is suitable for distortion correction and camera parameter calibration of three-dimensional DIC methods. Additionally, the disturbances from the external environment, such as light, vibration and airflow, also affect the measurement accuracy of DIC methods. In order to reduce the measurement error caused by the environment, some interferences such as monochromatic light are employed in the experiment and some algorithmic methods are also proposed by researchers. For instance, Pan et al. proposed a method that pre-smoothing the speckle images with a $5 \times 5$ pixels Gaussian low-pass filter before correlation analysis in which both numerical simulations and experiments reveal that the proposed technique could reduce the bias error for both noisy and noiseless images. The significant reduction of the bias error by using Gaussian pre-filtering is shown in Figure 5 (Pan, 2013). Except for disturbances from the environment, the undesired noise could also stem from measurement devices, such as photon noise and thermal noise. For these noises introduced by measurement devices, the use of a high-quality camera with better imaging effects could be helpful and also larger subset could be selected to reduce the influence of such noise.
7. DIC applications in manufacturing

Cutting: DIC technique has a broad application prospect in the research of cutting mechanism, notable examples including (1) observing the formation process of continuous chip and the propagation of crack via DIC, which provides an intuitive understanding of the cutting process; (2) DIC technique could clearly obtain physical quantities such as shear angle, tool radius, tool contact length, etc., which could be used as a reliable basis of theoretical research; (3) further processing from the displacement field in the cutting deformation area could obtain a series of useful variables and results such as the strain field, strain rate field, plastic strain field, etc. and (4) DIC technique offers an experimental method for deepening the understanding of the cutting behavior of new composite materials whose constitutive parameters are difficult to obtain, etc.

To date, the research of the cutting process by using the DIC technique is mainly focused on two conditions: studying low-speed cutting with a high-speed camera and high-speed cutting observation with a double-frame camera. For instance, Davis et al. investigated the chip-formation mechanism using the DIC technique with an *in situ* high-speed camera in which the chip morphology is characterized according to its cross-sectional geometry using different cutting speeds (Davis et al., 2018a). Also, Davis et al. further studied the strain and strain rate progression with the primary shear zone during chip formation based on the accurate measurement provided by the DIC technique with a high-speed camera. The experimental setup is shown in Figure 6(a) and (b), and shear strain distribution along the chip flow direction at a cutting speed of 0.5 m/s is shown in Figure 6(d) (Davis et al., 2018b). Due to the limitations of the performance of high-speed cameras, only the cutting process with relatively low-cutting speeds could be analyzed by using DIC, which hinders the application of DIC in practice. Therefore, some researchers have adopted a double-frame camera to observe the cutting process. The exposure time of the double-frame camera could

![Figure 5](https://example.com/figure5.png)

(a) Absolute difference in \(u\)-displacement (left) and \(v\)-displacement (right) fields measured by NR algorithm using quintic B-spline interpolation without Gaussian pre-filtering and quintic B-spline interpolation with Gaussian pre-filtering

(b) Absolute difference in \(u\)-displacement (left) and \(v\)-displacement (right) measured by NR algorithm using bicubic interpolation with Gaussian pre-filtering and quintic B-spline interpolation with Gaussian pre-filtering (Pan, 2013)
reach the order of one microsecond, and thus, the cutting process with a relatively high speed could be photographed. For instance, Baizeau et al. applied DIC with a double-frame camera to measure cutting forces at camera acquisition frequency. Subsequently, based on measurement results, the change of cutting forces is investigated when chip segments are formed (Baizeau et al., 2016). Further, Baizeau et al. used a high-speed double-frame imaging device with pulsed laser lighting to obtain sharp and highly resolved images during orthogonal cutting tests performed in an aluminum alloy in which the kinematic fields engendered by the cutting process are determined. The resultant surface textures after specimens were blasted with glass micro-beads having diameters of 50–100 μm under different blasting pressures (Baizeau et al., 2017) and (d) the shear strain rate distribution for the five stages of deformation during the formation of a single saw-tooth segment at a cutting speed of 0.5 m/s (Davis et al., 2018b). In general, compared with the traditional measurement method, the DIC technique is more suitable for the measurement during the cutting process because the cutting behavior has the features of small occurrence, severe deformation, short cutting process time, etc. The ability of DIC that could measure the chip formation process, including the intermediate quantity (e.g. strain and strain rate) in the cutting process, makes it possible to improve the quality of the workpiece, optimize the parameters and guide the production in the cutting process. Although the DIC technique offers some insight into the chip-formation mechanism, difficulties arise in identifying key features for high-speed cutting. Besides, the DIC technique
is unsuitable for the estimation of shear strain and shear strain rate when the sliding during chip formation is not a continuous deformation process, i.e., brittle machining.

**Welding:** In the field of welding, DIC is mainly used in the analysis of the welded joint, including (1) uniaxial tensile measurement of welded joints for the study of constitutive behavior; (2) analysis of crack strain field of welded joint for studying fracture behavior; (3) analysis of welding thermal deformation field to study the residual stress evolution of the joint, etc.

The application of DIC technique to the study of the constitutive relationship of welded joints began in 1999; Reynolds and Duvall presented a series of tensile tests of aluminum alloy specimens that are spliced by friction welding (Reynolds and Duvall, 1999). This work has been shown that if the property gradients in a weld are not too steep, then the constitutive properties of the micro-structural regions within a weld can be deduced from a single tensile test coupled with the DIC full-field displacement technique. Subsequently, Genevois et al. investigated the effect of the microstructure heterogeneity on the global and local tensile properties of friction-stir-welded joints in aluminum alloys via the DIC technique (Genevois et al., 2006). Lockwood et al. examined the global and local mechanical response of friction-stir-welded AA2024 experimentally and numerically and full-field strain measurements were obtained on transversely loaded tensile specimens via the DIC technique. The microstructure corresponding to the 2024 friction stir welding is shown in Figure 7(c) (Lockwood et al., 2002).

Leitão et al. presented the characterization of the constitutive behavior of friction stir welds based on the DIC technique in which the constitutive behavior of different weld regions was assessed from local tensile stress-strain curves. Transverse tensile specimen, strain maps, stress-strain curves and hardness profile for the S55 weld are shown in Figure 7(d) and (e) (Leitão et al., 2012).

Some researchers have also applied the DIC technique in fatigue tests, such as the crack growth analysis in welded joints. For instance, Chen et al. proposed the strategy that using the...
DIC technique coupled with thermo-elastic stress analysis to monitor the crack propagation process of T-joint specimens during the fatigue test (Chen et al., 2018). Corigliano et al. carried out static tensile and fatigue tests on butt-welded specimens made of S355 steel in which two full-field techniques were applied during the tests: DIC and infrared thermography techniques (Corigliano et al., 2017). The welded specimen and experimental setup are shown in Figure 7(a) and (b), respectively.

The DIC technique has also been employed to study the residual stress evolution of the welded joint. Xu et al. presented an incremental cutting method for evaluating the longitudinal residual stresses in the butt-welded thin plate by employing the DIC measurement technique (Xu and Bao, 2017). Kubit analyzed the strain distribution and residual stress of joints welded with the friction-stir-welding method after shot peening treatment in which the three-dimensional DIC method is used (Kubit et al., 2020). Generally, the DIC technique not only overcomes the problem that the deformation of the high-temperature weld area cannot be measured in real time, but also provides a validation method for numerical simulation theory. Although DIC methods have great advantages over the conventional measurement methods (e.g. heat-resisting strain gage) in the welding process, some challenges still remain for delivering the full potential in the welding field, including the effect of intense arc, the ablation of the speckle pattern owing to high temperature, oxidation of weldment surface interferes with image matching, etc.

**Forming:** In recent years, the application of the DIC technique has become increasingly popular in the forming process because it allows automatic evaluation of strains without tedious measurement of circle grids (Silva et al., 2015). Especially for the experimental characterization of the formability limits, the DIC technique has the additional advantage of avoiding manual intervention that usually leads to undesired measurement errors. In most cases, DIC is applied in the research of sheet metal forming for determining the plastic strain ratio of sheet metal and obtaining a reliable forming limit diagram (FLD) that both are important tools to evaluate the workability of metal sheets. For instance, Huang et al. determined the forming limit curve that is a key component in an FLD of sheet metal by using the DIC technique (Huang and Shi, 2017). Decultot et al. reported the development of strain fields encountered in incremental forming and evaluated the material formability on several formed shapes in single point incremental forming that is a promising sheet metal forming process for prototyping and small batches (Decultot et al., 2010). In order to obtain a more accurate FLD of the specimen, it is necessary to analyze the strain path during the deformation process. Besides, Mercedes et al. examined the geometric accuracy and thickness distributions using the DIC technique for studying the performance of multistage incremental sheet forming in formability, accuracy and uniform level of sheet thickness. The experimental setup, the image of the form and the corresponding 3D thickness model based on DIC data are shown in Figure 8(a–c), respectively (Mercedes et al., 2019). Wang et al. compared several different DIC procedures to establish an FLD and proposed a DIC-based time-dependent measurement method for the forming limit strains. This procedure is considered as more accurately defining the onset of necking and the boundary of safe deformation of an FLD as shown in Figure 8(e) (Wang et al., 2014). Compared with the conventional strain gage measurement that could only acquire the strain of fractural moment, the DIC method could measure the strain in the whole deformation process of any point in the specimen. For example, Cramer et al. quantified forming limits and retained austenite transformation in Q&P 1080 steel as a function of plastic strain levels for three different strain paths as shown in Figure 8(f) (Cramer et al., 2018).

Besides, the DIC technique has been also used in bulk metal forming, but the utilization has been limited to the determination of the stress-strain curves. Magrinho et al. studied the formability limits by fracture obtained from standard bulk metal forming tests performed with cylindrical, tapered and flanged specimens in which DIC was used to determine strain...
paths and immersion of steel specimens (Magrinho et al., 2018). Except for sheet and bulk metal forming, the application of the DIC technique in tube forming has also been reported. Cristino et al. made use of DIC technique, thickness measurements and force-displacement
evolutions to obtain the strain loading paths and the strain values at the onsets of failure by necking and fracture in tube forming (Cristino et al., 2019). Additionally, DIC technology has been used in some advanced forming processes, such as electromagnetic forming (EMF) that can improve the forming limit under room temperature. Deng et al. adopted DIC technology to calculate the full-field displacement, velocity, strain and strain rate with two high-speed cameras in the EMF process as shown in Figure 8(d) (Deng et al., 2019).

Typically, the DIC method is non-contacting and able to complete the measurement of the strain data of a specimen within a few minutes in the forming process. Besides, the DIC technique can not only measure the strain of the final state of sheet metal forming, but also can quickly and intuitively measure the strain distribution of the specimen surface during the entire forming process. Also, it could overcome the many shortcomings of conventional measurement methods, such as difficulty to repeat positioning, complicated procedures, time-consuming, unable to in situ measure, etc. Despite the rising popularity of the DIC, there remain some major technical challenges during the DIC data analysis for metal forming; for instance, it is hard to precisely pinpoint strains at the onset of localized necking.

**Additive manufacturing.** With the ever-growing demands of high-performance products with low lead times and more customized products, additive manufacturing has attracted more and more attention. However, in the manufacturing process, components are usually accompanied by some flaws such as shape deviations, cracking, and residual stresses, due to rapid heating, solidification, etc., which directly affects the mechanical performance of the components. In order to improve or avoiding the flaws mentioned above, researchers try to glean the mechanical properties of printed specimens via accurate measurement and then use these data as a basis to guide the optimization of the parameters in the manufacturing process. As a remarkable measurement method that takes advantage of robust, wide dynamic range and is not affected by rigid body motions and ambient vibrations, the DIC technique has been widely applied into advanced additive manufacturing for obtaining displacements and strains of printed components. Biegler et al. employed the DIC technique along with optical filters to measure in situ distortions on a wall geometry produced with laser metal deposition (LMD), experimental setup and in situ images are shown in Figure 9(a–c) (Biegler et al., 2018). In this work, the suitability of the DIC technique for measurements on an AM sample is shown and the potential for the validated numerical model as a predictive tool to reduce trial-and-error and improve part quality is evaluated. Ocelik et al. measured the in situ displacements and strains occurring on the substrate underside during a single laser metal deposition path, which provides very useful information concerning laser surface treatment and laser cladding that could help to optimize the laser cladding parameters and suppress the formation of high-level internal strains (Ocelik et al., 2009). Wu et al. explored the ability of DIC used in conjunction with sectioning to measure deformations occurring in selective laser melting (SLM) samples due to the removal from the substrate plate after processing (Wu et al., 2014). Additionally, as advanced non-contact instrumentation, DIC does not depend on the size of the specimen, which provides greater versatility for large additively manufactured components. For instance, Schnitker et al. verified the feasibility of using the DIC technique as a key enabler for robust data collection of strain measurements of large 3D printed components (Schnitker et al., 2019). Notably, DIC measurement combined with the finite element method (FEM) simulation could provide experimental support for the mechanical feasibility of a 3D printed specimen. For instance, Sutradhar et al. examined the feasibility of implants designed by the topology optimization method for craniofacial reconstructive surgery using DIC and FEM; the experimental setup and strain distribution comparison between DIC and FEA are shown in Figure 9(d) and (e) (Sutradhar et al., 2014). In general, DIC could capture full-field strain data with a good resolution on the surface of the model with complex geometries and inhomogeneity from images in the additive manufacturing process. Besides, the DIC technique could also be used for data collection
of strain measurements of large 3D-printed parts. Even though DIC is a powerful instrument for the study of additive manufacturing, it is hard to involve acquired information into the system which directly controls the process in a feedback loop due to a time delay caused by limited heat transfer speed.

8. Conclusion and prospects
After more than 30 years of development, DIC has been successfully used in a wide range of fields, providing robust and accurate measurements. In this review, the historical development of DIC, the advantages of DIC and its measurement construction have been systematically reviewed. Then, the basic principles have been elaborated in detail. The possible error sources of the DIC technique are also discussed and some suggestions are given for improving the measurement accuracy. So far, the DIC technique has been widely applied in the manufacturing area, including cutting, welding, forming, additive manufacturing, etc. due to its high performance.

With the ever-growing quality of industrial cameras and the development of relevant algorithms, the measurement accuracy of DIC has been constantly improved, and it has become one of the most versatile and powerful tools of deformation measurement in manufacturing. Although tremendous progress has been made, some challenges still exist when high-performance DIC measurements are required, especially for intelligent manufacturing. Specifically, these challenges mainly focus on the following aspects.

The measurement of a specimen with poor natural texture or without speckle pattern: On some occasions, it is not allowed or impossible to make artificial speckle patterns on the specimen. Problems may arise in the optical system of the DIC measurement due to the presence of natural textures that can interfere with the image analysis. This can affect the accuracy of the measurements, especially in cases where high spatial resolution is required. Solutions to this challenge include using different illumination techniques or applying specific filters to enhance the contrast between the specimen and the background.

Figure 9. (a) Schematic experimental setup for acquiring images of the laser-illuminated and patterned sample during LMD; (b) photograph of the setup after welding; (c) in situ image acquired by the left DIC camera in which patterned area is well visible even during welding, as the bright process is shielded by the optical filter (Biegler et al., 2018); (d) the configuration of the mechanical testing and data-capturing cameras and (e) vertical strain distribution comparison between FEA (left) and mechanical testing by DIC (right) (Sutradhar et al., 2014)
surface of the specimen, which leads to the infeasibility of measurement using DIC, because there is a lack of sufficient texture information to support accurate tracking. Therefore, solving the measurement of specimens with low natural texture could greatly improve the application range of DIC.

The measurement of the kinematic field tightly coupled with the thermal field at high temperatures: During the manufacturing process, it is accompanied by evitable changes in the temperature field, especially for mechanical testing at high temperatures and material processing at high temperatures. Therefore, it is important to measure the kinematic field coupled with the thermal field of the specimen for quality control and parameter optimization in the manufacturing process at high temperatures. Although many researchers have made great efforts on this topic and many measurement methods are proposed for obtaining both kinematic and thermal fields, such as using two different imaging systems to observe two different surfaces of the specimen (Srinivasan et al., 2012) and using two imaging systems to observe the kinematic and thermal fields on the same specimen surface (Bodelot et al., 2009), however, there are some problems with these methods, including the inconsistency of space and time coordinates in the two imaging devices and the high cost and instability caused by the combination of two imaging devices, and the surface of the specimen cannot simultaneously satisfy the measurement of the two fields. Taking into account the above disadvantages, a few researchers tried to obtain simultaneously kinematic and thermal fields using a single type of camera (Maynadier et al., 2012; Orteu et al., 2008). Although preliminary exploration has been done, the problem that the DIC and infrared thermography have conflicting requirements for the specimen surface has not been addressed (Zhang et al., 2019a, b).

Adaptively select the subset size and shape function on different occasions: As mentioned before, on the one hand, the subset size should be big enough so that there is a sufficiently distinctive intensity pattern to support the reliable analysis of correlation; on the other hand, the corresponding shape function should accurately approximate local deformation within the target subset in order to reduce the systematic errors caused by under-matched shape functions or random errors caused by over-matched shape functions. There is still a lack of the mechanism of adaptively selecting the subset and shape function, since the actual deformation occurring in each subset cannot be obtained in advance. Besides, in intelligent manufacturing with high requirements for intelligence and automation, the measurement technique needs to be sufficiently intelligent and automated to cope with different occasions. Thus, the adaptive selection of optimal subset size and shape function for subset matching is important for the application of the DIC technique in intelligent manufacturing.

The integration with modern design and simulation tools: As mentioned above, intelligent manufacturing imposes a high requirement in automation. The combination of DIC with computer-aided design (CAD) technology and FEM could provide the designing scheme, feasibility analysis and accurate measurement of products at once, which will greatly improve the automation and efficiency of intelligent manufacturing systems.

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