A mathematical simulation of flow regulation in vascular networks is used to investigate the interaction between arteriolar vasoconstriction due to sympathetic nerve activity (SNA) and vasodilation due to increased oxygen demand. A network with 13 vessel segments in series is used, each segment representing a different size range of arterioles or venules. The network includes five actively regulating arteriolar segments with time-dependent diameters influenced by shear stress, wall tension, metabolic regulation, and SNA. Metabolic signals are assumed to be propagated upstream along vessel walls via a conducted response. The model exhibits functional sympatholysis, in which sympathetic vasoconstriction is partially abrogated by increases in metabolic demand, and sympathetic escape, in which SNA elicits an initial vasoconstriction followed by vasodilation. In accordance with experimental observations, these phenomena are more prominent in small arterioles than in larger arterioles when SNA is assumed to act equally on arterioles of all sizes. The results imply that a mechanism based on the competing effects on arteriolar tone of SNA and conducted metabolic signals can account for several observed characteristics of functional sympatholysis, including the different responses of large and small arterioles.

Keywords: sympathetic nerve activity, microvascular flow regulation, mathematical model, exercise

INTRODUCTION

Local regulation of blood flow is critical for coordinating perfusion with local metabolic demand. Even under conditions of adequate overall organ blood flow, impairment of local regulation can lead to areas of inadequate oxygen delivery and impaired oxygen extraction. During flow regulation, redistribution of blood flow is achieved primarily by diameter changes due to contraction or relaxation of vascular smooth muscle in small arteries and arterioles, which result in large changes in resistance and flow according to Poiseille's law (Secomb, 2008). Vascular tone is modulated by local concentrations of vasodilatory metabolites, autonomic influences, hemodynamic factors, and conducted responses from downstream vessels (Segal, 2005). Responses to hemodynamic factors include vasodilatation in response to increasing wall shear stress (Pohl et al., 2000) as well as vasoconstriction in response to increases in transmural pressure (myogenic response) (Schubert and Mulvany, 1999).

Flow regulation during exercise additionally involves arteriolar dilation in active muscles due to metabolic factors, together with increased sympathetic stimulation causing vasoconstriction. The vasodilatory response of arterioles to hypoxia is thought to be due to the release of various metabolites from endothelium, tissue and erythrocytes in response to low oxygen levels (Davis et al., 2008). These local responses are augmented by communication of the generated signals along vessel walls, causing upstream vasodilation that increases oxygen delivery to hypoxic vascular beds (Segal and Jacobs, 2001; Secomb and Pries, 2002). Both upstream and downstream conduction of vasomotor signals have been demonstrated (Segal, 2000; Diep et al., 2005). Transmitted via gap junctions between endothelial and vascular smooth muscle cells (Gustafsson and Holstein-Rathlou, 1999), conducted responses are propagated over distances of order 1 mm or more (Bearden et al., 2004). Conducted responses have been shown to involve ATP sensitive potassium channels (Cohen and Sarelis, 2002) and can occur in the absence of erythrocytes (Ngo et al., 2010). Calcium-activated potassium channels have also been implicated (Bheringer et al., 2013). Upstream conducted responses communicate the need for increased local blood flow to the vessels supplying a hypoperfused area and appear to be a critical component of flow regulation. Diffusive interactions between paired arterioles and venules may also play a role in coordinating arteriolar diameters with tissue needs (Hester and Hammer, 2002).

Sympathetic vasoconstriction is largely mediated via activation of α-adrenoreceptors on smooth muscle (Joyner and Casey, 2014). Adrenergic innervation of the arteriolar tree has been observed to extend to the level of terminal arterioles (Marshall and Hebert, 1986). During exercise, sympathetic vasoconstriction serves to maintain mean arterial pressure despite increased flow to active muscles (Laughlin et al., 2012). Attempts to increase oxygen delivery during exercise by pharmacologic vasodilation have resulted in either no improvement in maximal aerobic capacity (Barden et al., 2007) or decreased oxygen extraction (Lundby et al., 2008). Despite an increase in blood flow, vasodilation via adenosine results in impaired metabolism-perfusion matching (i.e., decreased extraction), likely due to shunting of blood to non-exercising tissue (Calbet et al., 2006; Barden et al., 2014).
et al. (2003) found that responses by both receptor subtypes were size-dependent. However, Rosenmeier et al., 1998; Sarelius and Pohl, 2010). One possible mechanism is the modulation of sympathetic vasoconstriction by vasodilatory metabolites (Marshall and Hebert, 1986; Joyner and Thomas, 2003; Thomas and Segal, 2004; Joyner and Casey, 2014), with the net effect of directing flow to metabolically active areas (Delp and Laughlin, 1998; Saltin et al., 1998; Sarelius and Pohl, 2010).

Experimental observations of the combined effects of sympathetic nerve activity (SNA) and muscle contraction were presented by VanTeeffelen and Segal (2003) in vessels of different caliber in hamster retractor muscle. At rest, sympathetic vasoconstriction resulted in a decrease in vessel diameter over approximately 2–3 s, reaching a steady state after about 20 s. The absolute diameter change was largest in feed arteries, while the relative diameter change was largest in third-order arterioles. The functional vasodilation that occurred with muscle contraction reached a steady state in approximately 1 min. It was found to increase from proximal to distal branches and to depend on the intensity of muscle contraction, indicated in terms of percent duty cycle (%DC) (VanTeeffelen and Segal, 2003). The effect of SNA on arteriole diameters was reduced during muscle contraction, demonstrating functional sympatholysis. In some instances, an initial constriction of the vessel during a period of SNA during muscle contraction was followed by a partial relaxation, an effect known as “sympathetic escape.” These effects depended on the location within the network. In feed arteries, vasoconstriction was relatively preserved, whereas a marked attenuation was seen at the level of third-order arterioles.

The mechanisms underlying this variation with vessel order are not definitely established. One hypothesis is that it results from variation of receptor subtypes. In some muscles, the sympathetic vasoconstriction of smaller vessels with higher concentrations of \( \alpha_2 \) adrenergic receptors appears to be more susceptible to inhibition by vasodilatory metabolites as compared to larger vessels with higher concentrations of \( \alpha_1 \) receptors (Anderson and Faber, 1991; VanTeeffelen and Segal, 2003). However, Rosenmeier et al. (2003) found that responses by both receptor subtypes were blunted in exercise. Furthermore, Moore et al. (2010) found that the distribution of receptor subtypes with vessel size is dependent on muscle type. These studies imply that variations with vessel size of receptor subtypes and their response to SNA may not be the primary reason for the dependence of sympatholysis on vessel size within the arteriolar tree.

The overall objective of the present study is to obtain improved quantitative understanding of flow regulation, including the effects of autonomic regulation. Toward this objective, a theoretical model for local blood flow regulation is developed that includes the multiple factors discussed above and their interactions. A simplified approach is used to describe network structure, in which vessels of different size ranges are represented by compartments in series, each compartment consisting of multiple identical vessels in parallel. This model allows simulation of the time-dependent responses of different orders of arterioles to SNA and functional vasodilation during exercise, and of the interactions between these stimuli, including functional sympatholysis and sympathetic escape.

The model presented here has potential applications for simulating and analyzing the regulation of blood flow under a range of physiological and pathological conditions in which autonomic regulation plays an important role, including exercise hyperemia and maldistribution of blood flow in sepsis. It provides a basis for modeling effects of autonomic regulation in heterogeneous network structures. In the present study, it is used to address the following hypotheses: (1) sympatholysis and sympathetic escape result from vasodilatory metabolic signals reaching the arterioles via conducted responses following sympathetic vasoconstriction; (2) the size-dependent variation of these phenomena results from variations in the strength of the metabolic signals reaching arterioles of different sizes via conducted responses.

**MATERIALS AND METHODS**

**MODEL OVERVIEW**

A theoretical model was developed to investigate the interaction of sympathetic activity and functional vasodilation in the arteriolar tree. It is based on the “representative segment model” (Ursino et al., 1998; Corneliessen et al., 2002; Arciero et al., 2008; Carlson et al., 2008) in which vessels within different classes are assumed to have identical characteristics and responses. The seven-segment model (with two vasoactive segments) utilized in the studies of Arciero et al. (2008) and Carlson et al. (2008) was extended to include 13 segments, including five vasoactive arteriolar segments (Figure 1) in order to correspond to the arteriolar network of the hamster retractor muscle studied in VanTeeffelen and Segal (2003). Oxygen transport was assumed to occur in arteriolar and capillary segments according to the parameters in Table 1.

Parameters for each compartment (including vessel length, vessel number, and flow rate) were determined by specifying wall shear stresses and pressure drops in each segment (Table 2). The resultant pressure-diameter relationships are consistent with experimental observations (Pries et al., 1995).

The model predicts diameter changes and oxygen delivery (perfusion) as a function of oxygen demand (consumption) and network perfusion pressure. Flow through the network is calculated assuming an overall pressure drop from the arteriolar inflow to the venular outflow. Arterioles are assumed to be vasoactive, whereas the capillary segments and venous vessels are assumed to act as fixed resistances (Arciero et al., 2008). Specific aspects of the model are discussed in the following sections.

**FLOW REGULATION**

The arterioles are assumed to regulate flow in response to metabolic, myogenic, shear-dependent and autonomic stimuli. Metabolic signals are assumed to be generated by release of ATP from erythrocytes at a rate that depends on oxyhemoglobin...
Figure 1 | Schematic diagram of representative segment model. Each compartment is assumed to contain an array of identical segments in parallel, representing a range of arteriole or venule sizes.

Table 1 | Values of model parameters related to oxygen transport and metabolic signaling.

| Parameter | Description                  | Value       | Units                | References                  |
|-----------|------------------------------|-------------|----------------------|-----------------------------|
| $M_0$     | Oxygen demand                | 1.0–8.28 cm$^3$O$_2$ cm$^{-3}$ min$^{-1}$ | Arciero et al., 2008        |
| $C_0$     | Oxygen carrying capacity     | 0.5 cm$^3$O$_2$ cm$^{-3}$ | McGuire and Secomb, 2001 |
| $H_T$     | Tube hematocrit              | 0.3 –       | Arciero et al., 2008  |
| $H_D$     | Discharge hematocrit         | 0.4 –       | Arciero et al., 2008  |
| $R_0$     | Maximal ATP release rate     | $1.4 \times 10^{-9}$ mol s$^{-1}$ cm$^{-3}$ | Bergfeld and Forrester, 1992 |
| $R_I$     | Effect of $S$ on ATP release | 0.891 –     | Bergfeld and Forrester, 1992 |
| $n$       | Hill parameter               | 2.7 –       | McGuire and Secomb, 2001 |
| $P_{H0}$  | Hill parameter               | 26 torr     | McGuire and Secomb, 2001 |
| $S(t)$    | Initial oxygen saturation    | 0.97 –      | Arciero et al., 2008  |
| $C_{ATP}(0)$ | Initial ATP concentration  | 0.5 μM     | Gonzalez-Alonso et al., 2002 |
| $k_d$     | Rate of ATP degradation      | $2 \times 10^{-4}$ cm s$^{-1}$ | Dull et al., 1992          |
| $\tau_d$  | Diameter time constant       | 1 s         | Johnson, 1980         |
| $\tau_a$  | Activation time constant     | 20 s        | Roy et al., 2012      |
| $L_{met}$ | Conduction length constant   | 1 cm        | Arciero et al., 2008  |
| $C_{meta}$ | Metabolic signal coefficient | 30 μM$^{-1}$ cm$^{-1}$ | Arciero et al., 2008     |

Table 2 | Values of structural and hemodynamic parameters in the reference state for the representative segment model used in the simulations.

| Parameter                  | A     | FA    | 1A    | 2A    | 3A    | TA    | TV    | 1V    | 2V    | 3V    | DV    | V     | Total |
|---------------------------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|
| Diameter, $D$, μm         | 100.7 | 60    | 37    | 25.8  | 15.6  | 9.7   | 6     | 14.93 | 24.63 | 43.19 | 65.21 | 109.4 | 183.7 |
| Wall shear stress, $\tau$, dyn cm$^{-2}$ | 55    | 55    | 55    | 55    | 55    | 55    | 55    | 10    | 10    | 10    | 10    | 10    | 10    |
| Pressure drop, $\Delta P$, mmHg | 10    | 15    | 10    | 10    | 10    | 15    | 0.18  | 1.15  | 1.09  | 0.93  | 8.96  | 6.94  | 8.76  |
| Number of segments, $n$   | 0.23  | 1     | 4.33  | 14.62 | 93.06 | 585.3 | 4337  | 585.3 | 93.06 | 14.62 | 4.33  | 1     | 0.23  |
| Segment length, $L$, cm   | 0.61  | 0.5453 | 0.2242 | 0.1563 | 0.0945 | 0.0588 | 0.0545 | 0.0588 | 0.0945 | 0.1563 | 0.2242 | 0.5453 | 0.61  | 3.433 |
| Velocity, $v$, cm$^{-1}$  | 3.053 | 1.976  | 1.201 | 0.7312 | 0.3141 | 0.1292 | 0.0456 | 0.0545 | 0.1260 | 0.2609 | 0.3866 | 0.5943 | 0.9174 |
| Viscosity, $\mu$, cP      | 2.27  | 2.09   | 2.12  | 2.43  | 3.41  | 5.16  | 9.05  | 3.42  | 2.44  | 2.07  | 2.11  | 2.30  | 2.50  |
| Vascular volume, % of tissue | 0.24  | 0.33   | 0.22  | 0.25  | 0.36  | 0.54  | 1.41  | 1.27  | 0.89  | 0.71  | 0.69  | 0.79  | 0.79  |

Values in bold are prescribed, and the remaining values are calculated based on geometric and hemodynamic considerations.
saturation (32, 37) and to be propagated upstream from all vessels to the arterioles via conducted responses. The specific assumed mechanism of metabolic response is not critical to the model, and other mechanisms providing sensitivity over a wide range oxygen levels would be expected to yield comparable results (Golub and Pittman, 2013). The diameter of each regulating segment is represented as a function of time by a model that incorporates vessel wall mechanics and vascular smooth muscle tone (Arciero et al., 2008; Carlson et al., 2008). This model is designed to represent the following key features of flow regulation by arterioles: (1) The vasoactive signal for tone generation depends on the balance between competing vasodilator and vasoconstrictor stimuli. (2) The level of vascular smooth muscle activation has maximal and minimal levels, and exhibits saturating behavior at high net levels of vasodilator or vasoconstrictor signals.

For each arteriolar segment, the generated wall tension \( T_{\text{total}} \) is assumed to consist of a passive component \( T_{\text{pass}} \) and an active component \( T_{\text{act}} \) in parallel such that

\[
T_{\text{total}} = T_{\text{pass}} + A \cdot T_{\text{act}}^{\text{max}}
\]

where the activation \( A \) characterizes the level of vascular tone in each segment. For a vessel of diameter \( D \), the passive component \( T_{\text{pass}} \) is given by

\[
T_{\text{pass}} = C_{\text{pass}} \exp \left[ \frac{C'_{\text{pass}}}{D/D_0 - 1} \right]
\]

where \( C_{\text{pass}} \) and \( C'_{\text{pass}} \) are constants and \( D_0 \) represents the passive vessel diameter at a pressure \( P = 100 \) torr (Carlson and Secomb, 2005; Carlson et al., 2008). The active component \( T_{\text{act}}^{\text{max}} \) generated by vascular smooth muscle is given by

\[
T_{\text{act}}^{\text{max}} = \pi r^2 C_{\text{act}} \exp \left[ - \left( \frac{D/D_0 - C_{\text{act}}'}{C_{\text{act}}''} \right)^2 \right]
\]

where \( C_{\text{act}}, C_{\text{act}}', \) and \( C_{\text{act}}'' \) are parameters characterizing the length dependence of force generation (Carlson and Secomb, 2005; Carlson et al., 2008). Values for the parameters describing vessel wall mechanics are given in Table 3.

The target activation \( A_{\text{total}} \) is calculated from

\[
A_{\text{total}} = \frac{1}{1 + \exp \left( -S_{\text{tone}} \right)}
\]

and satisfies \( 0 \leq A_{\text{total}} \leq 1 \), where \( A_{\text{total}} = 0 \) represents absence of vascular tone and \( A_{\text{total}} = 1 \) represents maximal vasoconstriction. The total vasoactive signal \( S_{\text{tone}} \) represents the net effect of the myogenic, shear-dependent, autonomic and metabolic responses on vascular smooth muscle tone:

\[
S_{\text{tone}} = C_{\text{myo}} T - C_{\text{shear}} \tau_{\text{wall}} + C_{\text{symp}} - S_{\text{CR}} + C_{\text{tone}}
\]

where \( T = PD/2 \) is the circumferential wall tension, \( \tau_{\text{wall}} \) is the wall shear stress, \( S_{\text{CR}} \) represents the conducted (metabolic) response signal and \( C_{\text{myo}}, C_{\text{shear}}, C_{\text{symp}}, \) and \( C_{\text{tone}} \) are constants (Carlson and Secomb, 2005; Arciero et al., 2008). The time-dependent behavior of the diameter \( D \) and activation \( A \) in each segment are calculated by integrating the system of equations

\[
\frac{dD}{dt} = \frac{1}{\tau_D} \left( T - T_{\text{total}} \right)
\]

\[
\frac{dA}{dt} = \frac{1}{\tau_A} \left( A_{\text{total}} - A \right)
\]

where \( T = PD/2 \), \( \tau_D \) and \( \tau_A \) are the respective time constants for changes in \( D \) and \( A \) and the subscript \( c \) refers to the control state (Carlson et al., 2008). In some cases, these solutions approach steady-state behavior, but oscillatory behavior is also possible (Arciero and Secomb, 2012).

### OXYGEN TRANSPORT

Oxygen transport in the network is calculated using a simplified model (Arciero et al., 2008). Zero-order oxygen uptake kinetics are assumed for a tissue sleeve of width 18.8 \( \mu \)m surrounding the feed artery and each arteriole and capillary, resulting in a linear decrease in oxygen saturation with distance until oxygen is fully depleted. The width of the sleeve corresponds to an overall capillary density of 500 \( \text{mm}^{-2} \), typical of skeletal muscle. The Hill equation is used to estimate oxygen saturation as a function of oxygen tension. Oxygen exchange is neglected in venous segments. Values for parameters governing oxygen transport are given in Table 1.

### CONDUCTED METABOLIC RESPONSE

Metabolic signals are assumed to be generated in all segments in response to the saturation-dependent release of ATP by erythrocytes (Ellsworth et al., 2009). Signals are assumed to be conducted upstream from all segments, including venules and capillaries, to the arterioles (Collins et al., 1998), where they influence the generation of vascular tone (Ellsworth et al., 2009). The local metabolic signal \( S_{\text{loc}} \) for each segment is:

\[
S_{\text{loc}} = C_{\text{meta}}^{\text{rbc}} \cdot C_{\text{ATP}}
\]

where \( C_{\text{ATP}} \) is the mean local ATP concentration and \( C_{\text{meta}}^{\text{rbc}} \) is a parameter describing the strength of the responses (see Table 1).

---

**Table 3 | Parameter values characterizing vascular smooth muscle properties for vasoactive segments.**

| Parameter | FA   | 1A   | 2A   | 3A   | TA   |
|-----------|------|------|------|------|------|
| \( D_0 \) \( \mu \)m | 173.1 | 125.3 | 95.41 | 62.98 | 41.35 |
| \( C_{\text{myo}} \), cm dyn\(^{-1} \) | 0.0079 | 0.0109 | 0.0143 | 0.0217 | 0.0331 |
| \( C_{\text{shear}} \), cm\(^2\) dyn\(^{-1} \) | 0.0258 | 0.0258 | 0.0258 | 0.0258 | 0.0258 |
| \( C_{\text{pass}} \), dyn cm\(^{-1} \) | 1154 | 834.9 | 636.0 | 419.8 | 275.6 |
| \( C_{\text{act}} \), dyn cm\(^{-1} \) | 7846 | 9138 | 9944 | 10.82 | 11.40 |
| \( C_{\text{act}}^{\text{max}} \) | 2671 | 1654 | 1106 | 598.1 | 320.8 |
| \( C_{\text{act}} \) | 0.6709 | 0.6991 | 0.7167 | 0.7358 | 0.7486 |
| \( C_{\text{act}}^{\text{max}} \) | 0.2765 | 0.3148 | 0.3387 | 0.3646 | 0.3819 |

Numerical values of the parameters above are derived from formulas in Carlson and Secomb (2005) and Carlson et al. (2008); see also Table 1 of Fry et al. (2013).
The conducted signal $S_{CR}$ (Equation 5) is assumed to act analogously to an electrical potential within the vessel wall, and is propagated upstream from the segment endpoint $x_{end}$ with exponential decay according to a length constant $L_{met}$ (Table 1), such that the conducted response $S_{CR}$ at a given point $x$ along the flow pathway in each segment is given by

$$S_{CR} = \int_x^{x_{end}} e^{-(y-x)/L_{met}} S_{loc}(y) dy \quad (9)$$

and is continuous at the transitions from each class of vessels to the next. This method is appropriate for simulating conducted responses in representative segment models (Arciero et al., 2008), where all segments in a given compartment are equivalent. For heterogeneous networks, a more complex approach using circumference-weighted currents can be used (Roy et al., 2012). In some simulations, the values of the metabolic signals $S_{CR}$ in each segment during SNA were artificially “locked” at the values that existed immediately prior to SNA. Comparisons with these simulations provided a basis for assessing the role of metabolic signals in sympatholysis.

**AUTONOMIC REGULATION**

The baseline diameter of arterioles is determined by the amount of muscle SNA at rest (Charkoudian et al., 2006). The effect of SNA increases above baseline on arteriolar tone is incorporated via the constant $C_{sym}$ in Equation 5. Values of $C_{sym}$ (1, 2, 4) were chosen corresponding to low, intermediate, and high (L, I, H) levels of SNA as generated by mean frequencies of 3, 6, and 12 Hz in the experiments of VanTeeffelen and Segal (2003). In simulations under resting conditions, the predicted decrease in diameter of first-order arterioles (1A) with L, I, and H levels of SNA ranged from 3 to 10 $\mu$m. This is comparable to the reductions of 4–14 $\mu$m observed experimentally (VanTeeffelen and Segal, 2003), suggesting that the values of $C_{sym}$ assumed in the model are appropriate.

**REFERENCE STATE**

Unlike the model of Arciero et al. (2008) and Carlson et al. (2008) which utilized a control state corresponding to moderate oxygen consumption, the reference state for the 13-segment representative segment model was chosen to correspond to resting conditions (Table 2). Resting diameters for arteriolar segments from feed arteries to third-order arterioles were specified based on observations of VanTeeffelen and Segal (2003). The diameter of the terminal arteriole was calculated as the geometric mean of the third-order arteriole and capillary diameters. Passive diameters were inferred by using interpolated ratios of resting to passive diameter for the vasoactive arteriolar segments in the model of Arciero et al. (2008). The values for $C_{tone}$ (Equation 5) used for each vasoactive compartment were determined in the reference state by setting the target activation $A_{total} = A$ as deduced from Equation 1 and calculating $S_{tone}$ from Equation 4.

**OXYGEN DEMAND**

The metabolic vasodilatory stimulus resulting from muscle contraction was assumed in the model to act via increased oxygen demand and resulting reductions in intravascular oxygen levels. Oxygen demand values of 1, 1.91, 4.64, and 8.28 cm$^3$O$$_2$ cm$^{-3}$ min$^{-1}$ were used to correspond to rest and to 2.5, 10, and 20% DC (contractile activity). The resulting steady-state diameters for vessels of different classes at different levels of consumption corresponded approximately to the experimentally observed values of VanTeeffelen and Segal (2003). Other mechanisms, such as release of potassium ions from contracting muscle, may also contribute to the metabolic response and could be included in this modeling approach (Lo et al., 2004).

**RESULTS**

Time-dependent simulations were performed for levels of SNA and contractile activity corresponding to the conditions in the experiments of VanTeeffelen and Segal (2003). Three levels of SNA and three levels of oxygen consumption were applied separately and in combination to investigate the interaction between SNA and contractile activity. Figure 2 shows the predicted time course of the diameters of the FA and 3A segments, under conditions corresponding to the experimental results shown in Figure 3 of VanTeeffelen and Segal (2003). In each case, a 30-s period of intermediate-level SNA is applied under resting conditions and during a period of increased oxygen consumption corresponding to muscle contraction. As expected, the model predicts vasoconstriction in response to SNA and vasodilation in response to increased oxygen demand in all cases. In the 3A segment, sympathetic escape is predicted both at rest and with each level of muscle contraction, as indicated by an initial vasoconstriction during SNA followed by a partial dilation. The model simulations show several features in common with experimental results (VanTeeffelen and Segal, 2003), including the prominent appearance of sympathetic escape in the 3A but not in the FA segment, and the occurrence of an after-dilation following the cessation of SNA. In the experiments (VanTeeffelen and Segal, 2003), one instance was seen of complete absence of vasoconstriction in response to SNA (in the 3A segment under contraction at 20% DC). According to the present model, such an effect would be possible due to a precise balance of opposing effects of SNA and metabolic dilation in a specific segment, but this did not occur with assumed parameter values.

Predicted diameter changes of each arteriolar segment with application of high SNA ($C_{sym} = 4$) are shown in Figure 3 for several levels of oxygen consumption. Changes are shown for diameters at the end of SNA relative to the diameters prior to the period of SNA. Since these baseline diameters increased with increasing oxygen demand, the results are presented in terms of both percent and absolute reductions. The predicted diameter reductions with high SNA are in the range of 10–30% in all cases. The smallest percentage changes are seen in the smaller arterioles at higher levels of oxygen consumption, consistent with the more prominent effect of sympatholysis under those conditions. In absolute terms, the reductions in diameter varied from about 2–20%, with larger reductions in the larger arterioles. Figure 3 also shows predicted results when the metabolic signal is “locked” at its value before SNA, eliminating any compensatory metabolic signal generated in response to sympathetic vasoconstriction. In that case, the percentage reductions in diameter are generally larger, as much as 60% in the TA, and show a...
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FIGURE 2 | Time-dependent diameter changes in feed arteries (FA) and third order arterioles (3A) in response to sympathetic nerve activity (shaded bars) at rest and with increased oxygen demand representing three levels of muscle contraction (unshaded bars). In all cases, results for intermediate levels of SNA (Csymp = 2) are shown. Assumed levels of oxygen demand were 1 at rest, and 1.91, 4.64, and 8.28 (all in units of cm³O₂ cm⁻³ min⁻¹) for the three levels of contraction (DC2.5, DC10, and DC20%).

A strong increase with muscle activation. Comparison of these sets of results implies that the variation of the conducted metabolic signal in response to reduction in flow plays a major part in moderating the contraction resulting from SNA.

The predicted effect of SNA on blood flow rate through the network is shown in Figure 4. As expected, the flow rate at the end of SNA increases with the level of contractile activity, and decreases with increasing SNA. Moderate decreases in flow with SNA are seen when normal metabolic responses are included (Figure 4A). If, however, the metabolic responses are fixed at their respective levels prior to the application of SNA, the effect of compensatory metabolic vasodilation can be demonstrated. Under such conditions (Figure 4B), extreme decreases of flow are seen, particularly at higher oxygen demand. These results show the role of metabolic signals in maintaining flow during functional sympatholysis.

The phenomenon of sympathetic escape can be quantified using an escape index (EI) (Boegehold and Johnson, 1988), given by

\[
EI = \frac{D_m - D_e}{D_m - D_0}
\]  

where \(D_0\) represents the diameter prior to SNA, \(D_m\) represents the minimum diameter during SNA, and \(D_e\) represents the diameter at the end of SNA. Figure 5 shows that EI is larger for smaller vessels as compared to larger vessels, and that EI increases with increasing oxygen demand.

The contributions to functional sympatholysis of the various factors determining stimuli contributing to vessel tone are examined in Figure 6. Contractile activity corresponding to 20% DC is assumed. According to Equation 5, \(S_{tone}\) is the sum of the components \(S_{myo} = C_{myo}T\), \(S_{shear} = -C_{shear}τ_{wall}\), \(S_{symp} = C_{symp}\), and \(S_{meta} = -SCR\), along with an additive constant. Figure 6 shows the changes in each of these components in terms of the difference between the value at the end of 30 s of high-level SNA and the value prior to SNA. The changes in \(S_{tone}\) are displayed in terms of \(-ΔS_{tone}\), such that higher values of this quantity represent vasodilation and lower values represent vasoconstriction. As Figure 6 shows, the vasoconstrictor effects of the SNA component \(S_{symp}\) are partially compensated by the metabolic vasodilator effect of \(S_{meta}\). This effect is strongest in the smaller arterioles, where \(S_{tone}\) is restored close to its pre-SNA level. As the metabolic signal is conducted upstream along the vessel walls, it gradually loses strength due to its distance-based decay (Equation 9). In the larger vessels, this results in a net vasoconstriction with SNA, i.e., \(-ΔS_{tone} < 0\). According to the model, this decay may be the cause of the reduced sympatholysis observed in the proximal arteriolar segments.

DISCUSSION

In exercising skeletal muscle, multiple mechanisms interact to increase perfusion, including increased cardiac output and peripheral vasodilation mediated by a range of metabolites. Sympathetic stimulation during exercise causes vasoconstriction of arterioles to actively contracting muscles, and plays a
critical role in perfusion-metabolism matching at the microcirculatory level (Joyner and Thomas, 2003; Calbet and Joyner, 2010). Functional sympatholysis has the effect of directing blood flow to metabolically active areas. Impaired functional sympatholysis (as seen in aging, immobilization, and pathological states such as hypertension) has been implicated as a cause of poor metabolism-perfusion matching in skeletal muscle, resulting in performance limitations (Saltin and Mortensen, 2012), with the implication that this can be rectified by training (Jendzjowsky and Delorey, 2013). Some of the changes associated with aging may be due to decreases in the length constant for conducted metabolic responses, limiting the extent of vasodilation (Behringer et al., 2013). Although the physiological importance of functional sympatholysis is well accepted, its mechanistic basis and its role in exercise hyperemia remain the subjects of debate (Pancheva et al., 2013; Joyner and Casey, 2014). One obstacle is the difficulty of isolating the effects of interacting regulatory mechanisms in experimental systems.

In this context, theoretical models offer a potentially useful approach, providing a quantitative framework for integrating
information about relevant mechanisms and examining their interactions. However, few previous theoretical studies have addressed the issue of autonomic regulation in the microcirculation. The present work uses a simplified model that nonetheless includes a number of important aspects of flow regulation in the microcirculation: (1) multiple mechanisms of flow regulation, including SNA; (2) a complete flow pathway, including arterioles of various sizes; (3) time-dependent behavior. The model approach builds on that developed previously (Arciero et al., 2008; Carlson et al., 2008). An advantage of this approach is that it provides a natural framework (Equation 5) for incorporating additional regulatory mechanisms, in this case the effect of SNA.

The main finding of this study is that the phenomenon of sympatholysis can be explained in terms of the negative feedback induced by metabolic flow regulation. When SNA is applied the resulting vasoconstriction results in a reduction in blood flow and impaired tissue oxygenation, which generates an upstream conducted vasodilator response that substantially compensates for the sympathetic vasoconstriction. A further finding is that a differential response to SNA based on vessel diameter need not be invoked to explain the observed dependence of sympathetic escape on arteriole size. In the model, the same sympathetic stimulus was applied to vessels independent of size, but the larger conducted metabolic signal in smaller vessels was responsible for functional sympatholysis. This arises as a consequence of the decay in the magnitude of the conducted metabolic response signal as it travels upstream to arterioles of successively increasing size. The decay rate may depend on the assumed length constant of the conducted response. Here \( L_{\text{net}} = 1 \text{ cm} \) was assumed (Arciero et al., 2008). The vasoconstriction due to SNA in feed arteries overcomes metabolic vasodilation at higher oxygen demand, resulting in persistent vasoconstriction throughout the period of SNA. In smaller arterioles under similar conditions, however, the initial vasoconstriction with SNA is followed by partial relaxation, consistent with the experimentally observed phenomenon of sympathetic escape. This implies that the relative magnitude of metabolic responses can account for observed characteristics of functional sympatholysis, including the different responses of large and small arterioles.

The development of a theoretical model for flow regulation and sympatholysis necessarily involves numerous simplifying assumptions that may not accurately reflect the actual system. While these assumptions do not negate the general conclusions stated above, they may limit the ability of the model to provide a quantitatively correct representation of the system. Metabolic vasodilation is assumed to result from an oxygen-dependent mechanism and responses to other metabolic stimuli are not explicitly represented. The representative segment model used herein does not take into account a number of effects that are present in heterogeneous vascular networks, specifically (1) variation in flow pathways; (2) phase separation in bifurcations and formation of plasma channels; (3) capillary recruitment; and (4) regional variation in oxygen content. Finally, the simplified oxygen transport model used here does not include diffusive interactions between neighboring vessels.

The present model assumes that the metabolic signal originates from saturation-dependent ATP release from erythrocytes. Previous work has shown that such a mechanism does not provide optimal metabolism-perfusion matching in heterogeneous networks (Roy et al., 2012; Fry et al., 2013), and has suggested that wall or tissue-derived signals are important in metabolic flow regulation. Here, however, a homogeneous network structure is assumed, such that the results are not highly dependent on the assumed mechanism of metabolic regulation. The erythrocyte-derived signal was assumed because it has previously been shown to give results in good agreement with experimental data in a representative segment model (Arciero et al., 2008). The model could be readily modified to incorporate alternative mechanisms (Roy et al., 2012; Fry et al., 2013). A further assumption of the model is that the generation and upstream conduction of the metabolic signal are instantaneous. This may not be the case if metabolite generation and diffusion are responsible for the metabolic response. Signals with various time-dependent behaviors, such as adenosine (Mortensen et al., 2009), potassium (Lo et al., 2004), calcium (Behringer et al., 2013), and nitric oxide (Casey et al., 2013; Golub and Pittman, 2013), have been proposed as regulators of metabolic vasodilation under conditions of increased oxygen demand and may contribute to the phenomenon of sympatholysis and escape. The time-dependent framework used in this model can readily be adapted to include the dynamics of metabolic signal generation to further investigate its interaction with SNA. The model provides a basis for investigating the interaction of metabolic and autonomic signals in pathological conditions such as sepsis, in which regional heterogeneity of oxygen demand, altered conduction of metabolic signals (Gustafsson and Holstein-Rathlou, 1999), and increased sympathetic activity are present.

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REFERENCES

Anderson, K. M., and Faber, J. E. (1991). Differential sensitivity of arteriolar alpha-1- and alpha-adrenoceptor constriction to metabolic inhibition during rat skeletal muscle contraction. *Circ. Res.* 69, 174–184. doi: 10.1161/01.RES.69.1.174

Arciero, J. C., Carlson, B. E., and Secomb, T. W. (2008). Theoretical model of metabolic blood flow regulation: roles of ATP release by red blood cells and conducted responses. *Am. J. Physiol. Heart Circ. Physiol.* 295, H1562–H1571. doi: 10.1152/ajpheart.00261.2008

Arciero, J. C., and Secomb, T. W. (2012). Spontaneous oscillations in a model for active control of microvessel diameters. *Math. Med. Biol.* 29, 163–180. doi: 10.1093/imammb/dqr005

Barden, J., Lawrenson, L., Poole, J. G., Kim, J., Wray, D. W., Bailey, D. M., et al. (2007). Limitations to vasodilatory capacity and VO2max in trained human skeletal muscle. *Am. J. Physiol. Heart Circ. Physiol.* 292, H2491–H2497. doi: 10.1152/ajpheart.01396.2006

Bearden, S. E., Payne, G. W., Chisty, A., and Segal, S. S. (2004). Arteriolar network architecture and vasomotor function with ageing in mouse gluteus maximus muscle. *J. Physiol.* 561, 535–545. doi: 10.1113/jphysiol.2004.068262

Behringer, E. J., Shaw, R. L., Westcott, E. B., Socha, M. J., and Segal, S. S. (2013). Aging impairs electrical conduction along endothelium of resistance arteries through enhanced Ca2+-activated K+ channel activation. *Arterioscler. Thromb. Vasc. Biol.* 33, 1892–1901. doi: 10.1161/ATVBAHA.113.301514
Boegehold, M. A., and Johnson, P. C. (1988). Periarteriolar and tissue PO2 during sympathetic escape in skeletal muscle. *Am. J. Physiol.* 254, H929–H936.

Calbet, J. A., and Joyner, M. J. (2010). Disparity in regional and systemic circulatory capacities: do they affect the regulation of the circulation? *Acta Physiol.* 199, 393–406. doi: 10.1111/j.1748-1796.2010.02125.x

Calbet, J. A., Lundby, C., Sander, M., Robach, P., Saltin, B., and Boushel, R. (2006). Effects of ATP-induced leg vasodilation on VO2 peak and leg O2 extraction during maximal exercise in humans. *Am. J. Physiol. Regul. Integr. Comp. Physiol.* 291, R447–R453. doi: 10.1152/ajpregu.00746.2005

Carlson, B. E., Arciero, J. C., and Secomb, T. W. (2008). Theoretical model of blood flow autoregulation: roles of myogenic, shear-dependent, and metabolic responses. *Am. J. Physiol. Heart Circ. Physiol.* 295, H1572–H1579. doi: 10.1152/ajpheart.00262.2008

Carlson, B. E., and Secomb, T. W. (2005). A theoretical model for the myogenic response based on the length-tension characteristics of vascular smooth muscle. *Microcirculation* 12, 327–338. doi: 10.1080/10739680590934745

Casey, D. P., Walker, B. G., Ranadive, S. M., Taylor, J. L., and Joyner, M. J. (2013). Conducted vasomotor responses: communication across the capillary bed. *Am. J. Physiol. Regul. Integr. Comp. Physiol.* 302, R1280–R1285. doi: 10.1152/ajpregu.00744.2001

Cohen, K. D., and Sarelius, I. H. (2002). Muscle contraction under capillaries in contracting muscles. *J. Physiol.* 547, 971–976. doi: 10.1113/jphysiol.2002.037937

Cornelissen, A. J., Dankelman, J., VanBavel, E., and Spaan, J. A. (2002). Balance of sympathetic activity on consecutive sections of microcirculation of mesentery and skeletal muscle. In *Microvascular Networks: Experimental and Theoretical Studies*, eds A. S. Popel and P. C. Johnson (Basel: Karger), 123–133.

McGuire, B. J., and Secomb, T. W. (2001). A theoretical model for oxygen transport in skeletal muscle under conditions of high oxygen demand. *J. Appl. Physiol.* 91, 2255–2265.

Moore, A. W., Jackson, W. F., and Segal, S. S. (2010). Regional heterogeneity of alpha-adrenoceptor subtypes in arteriolar networks of mouse skeletal muscle. *J. Physiol.* 588, 4261–4274. doi: 10.1113/jphysiol.2010.194993

Mortensen, S. P., Nyberg, M., Thaning, P., Saltin, B., and Hellsten, Y. (2009). Adenosine contributes to blood flow regulation in the exercising human leg by increasing prostaglandin and nitric oxide formation. *Hypertension* 53, 993–999. doi: 10.1161/HYPTENSIONAHA.109.130880

Moore, A. W., Jackson, W. F., and Segal, S. S. (2013). Regional heterogeneity of alpha-adrenoceptor subtypes in arteriolar networks of mouse skeletal muscle. *J. Physiol.* 588, 4261–4274. doi: 10.1113/jphysiol.2010.194993

Mortensen, S. P., Nyberg, M., Thaning, P., Saltin, B., and Hellsten, Y. (2009). Adenosine contributes to blood flow regulation in the exercising human leg by increasing prostaglandin and nitric oxide formation. *Hypertension* 53, 993–999. doi: 10.1161/HYPTENSIONAHA.109.130880

Ngo, A. T., Jensen, J. J., Riemann, M., Holstein-Rathlou, N., and Torp-Pedersen, C. (2010). Oxygen sensing and conducted vasomotor responses in mouse cremaster arteries in situ. *Pflugers Arch.* 460, 41–53. doi: 10.1007/s00424-010-0837-x

Pancheva, A. V., Panchev, V. S., and Pancheva, M. V. (2013). Functional sympathetic in the present concept does not exist: arteriovenous pumping, supplied by capillary pumps, explains immediate exercise hyperemia. *J. Appl. Physiol.* 114, 428. doi: 10.1152/japplphysiol.01391.2012

Pohl, U., de Wit, C., and Goe, T. (2000). Large arterioles in the control of blood flow: role of endothelium-dependent dilation. *Acta Physiol. Scand.* 168, 503–510. doi: 10.1046/j.1365-201X.2000.01007.x

Pries, A. R., Secomb, T. W., and Gaethgens, P. (1995). Design principles of vascular beds. *Circ. Res.* 77, 1017–1023. doi: 10.1161/01.RES.77.5.1017

Remmersnyder, J. P., Mitchell, J. H., and Sarnoff, S. J. (1962). Functional sympatholysis during muscular activity. Observations on influence of carotid sinus on oxygen uptake. *Circ. Res.* 11, 370–380. doi: 10.1161/01.RES.11.3.370

Rosenmeier, J. B., Dinenno, F. A., Fritzlar, S. J., and Joyner, M. J. (2003). alpha1- and alpha2-adrenergic vasoconstriction is blunted in contracting human muscle. *J. Physiol.* 547, 971–976. doi: 10.1113/jphysiol.2002.037937

Roy, T. K., Pries, A. R., and Secomb, T. W. (2012). Theoretical comparison of wall-derived and erythrocyte-derived mechanisms for metabolic flow regulation in heterogeneous microvascular networks. *Am. J. Physiol. Heart Circ. Physiol.* 302, H1945–H1952. doi: 10.1152/ajpheart.01176.2011

Saltin, B., and Mortensen, S. P. (2012). Inefficient functional sympatholysis is an overlooked cause of malperfusion in contracting skeletal muscle. *J. Physiol.* 590, 6269–6275. doi: 10.1113/jphysiol.2012.241026

Saltin, B., Radegran, G., Koskolou, M. D., and Roach, R. C. (1998). Skeletal muscle blood flow in humans and its regulation during exercise. *Acta Physiol. Scand.* 162, 421–436. doi: 10.1046/j.1365-201X.1998.00702.x

Schubert, R., and Mulvany, M. J. (1999). The myogenic response: established facts and attractive hypotheses. *Clin. Sci.* 96, 313–326. doi: 10.1042/CS19980403

Secomb, T. W. (2008). Theoretical models for regulation of blood flow. *Microcirculation* 15, 765–775. doi: 10.1080/10739680802350112
Seccomb, T. W., and Pries, A. R. (2002). Information transfer in microvascular networks. *Microcirculation* 9, 377–387. doi: 10.1038/sj.mn.7800146
Segal, S. S. (2000). Integration of blood flow control to skeletal muscle: key role of feed arteries. *Acta Physiol. Scand.* 168, 511–518. doi: 10.1046/j.1365-201x.2000.00703.x
Segal, S. S. (2005). Regulation of blood flow in the microcirculation. *Microcirculation* 12, 33–45. doi: 10.1080/10739680590895028
Segal, S. S., and Jacobs, T. L. (2001). Role for endothelial cell conduction in ascending vasodilatation and exercise hyperaemia in hamster skeletal muscle. *J. Physiol.* 536, 937–946. doi: 10.1111/j.1469-7793.2001.00937.x
Thomas, G. D., and Segal, S. S. (2004). Neural control of muscle blood flow during exercise. *J. Appl. Physiol.* 97, 731–738. doi: 10.1152/japplphysiol.00076.2004
Ursino, M., Colantuoni, A., and Bertuglia, S. (1998). Vasomotion and blood flow regulation in hamster skeletal muscle microcirculation: a theoretical and experimental study. *Microvasc. Res.* 56, 233–252. doi: 10.1006/mvre.1998.2106
VanTeeffelen, J. W., and Segal, S. S. (2003). Interaction between sympathetic nerve activation and muscle fibre contraction in resistance vessels of hamster retractor muscle. *J. Physiol.* 550, 563–574. doi: 10.1113/jphysiol.2003.038984

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