The inefficiency of satellite accretion in forming extended star clusters

Paolo Bianchini,1*† Florent Renaud,2,3 Mark Gieles2 and Anna Lisa Varri4

1 Max-Planck Institute for Astronomy, Koenigstuhl 17, D-69117 Heidelberg, Germany
2 Department of Physics, University of Surrey, Guildford GU2 7XH, UK
3 Laboratoire AIM Paris-Saclay, CEA/IRFU/SAp, Université Paris Diderot, F-91191 Gif-sur-Yvette Cedex, France
4 School of Mathematics and Maxwell Institute of Mathematical Sciences, University of Edinburgh, King’s Buildings, Edinburgh EH9 3JZ, UK

Accepted 2014 November 4. Received 2014 November 3; in original form 2014 October 15

ABSTRACT
The distinction between globular clusters and dwarf galaxies has been progressively blurred by the recent discoveries of several extended star clusters, with size (20–30 pc) and luminosity (−6 < \( M_\odot \) < −2) comparable to the one of the faint dwarf spheroidals. In order to explain their sparse structure, it has been suggested that they formed as star clusters in dwarf galaxy satellites that later accreted on to the Milky Way. If these clusters form in the centre of dwarf galaxies, they evolve in a tidally compressive environment where the contribution of the tides to the virial balance can become significant, and lead to a supervirial state and subsequent expansion of the cluster, once removed. Using N-body simulations, we show that a cluster formed in such an extreme environment undergoes a sizable expansion, during the drastic variation of the external tidal field due to the accretion process. However, we show that the expansion due to the removal of the compressive tides is not enough to explain the observed extended structure, since the stellar systems resulting from this process are always more compact than the corresponding clusters that expand in isolation due to two-body relaxation. We conclude that an accreted origin of extended globular clusters is unlikely to explain their large spatial extent, and rather favour the hypothesis that such clusters are already extended at the stage of their formation.

Key words: methods: numerical – globular clusters: general.

1 INTRODUCTION
In recent years, a number of low-luminosity stellar systems were discovered around galaxies populating the transition region between low-luminosity dwarf spheroidal galaxies (dSphs) and globular clusters (GCs) in the luminosity–size parameter space. These stellar systems, with a luminosity between \(-6 < M_\odot < -2\) and a half-light radius of about \(20–30\) pc, are often referred to as extended clusters. In the Milky Way (MW), the known objects are Pal 4, Pal 14, AM 1 (Mackey & van den Bergh 2005; Harris 2010), and several extragalactic ones (Brodie & Larsen 2002; Huxor et al. 2014; Mackey et al. 2013). They are preferentially found in the outer haloes of galaxies and are characterized by a more diffuse structure than typical GCs of similar luminosity. Therefore, their intermediate size, between the regime of dSphs galaxies and the bulk of GCs, makes them intriguing objects, crucial for the understanding of the differences and similarities of the formation of low-mass stellar systems.

Extended clusters have half-mass relaxation times slightly larger than their age, which makes it difficult to explain their sizes by expansion driven by two-body relaxation (Gieles, Heggie & Zhao 2011). The debate on the nature of these objects was recently enhanced by the discovery of the peculiar MW extended stellar system Laevens/I/Crater (half-light radius between 20 and 30 pc), whose classification as a GC or a dSph is still debated (Belokurov et al. 2014; Laevens et al. 2014). Moreover, the complexity of their internal dynamics is not fully understood yet. Frank, Grebel & Küpper (2014) found the surprising evidence of mass segregation in Pal 14. The current relaxation time of this extended cluster exceeds the Hubble time and therefore is too long to explain the settling of segregation only through dynamical evolution. The combined effect of primordial mass segregation and dynamical evolution could explain the structure of this cluster (Haghi et al. 2014). Therefore, further studies of the internal properties of such stellar systems are indeed crucial to unveil their origin.

The presumed origin of such extended clusters includes three main mechanisms: (1) they genuinely formed extended (this requires a formation environment with a high Mach number, which is appropriate to dwarf galaxies; Elmegreen 2008); (2) they formed through the merging of two or more star clusters (Fellhauer & Kroupa 2002; Assmann et al. 2011); (3) they were born as compact

*E-mail: bianchini@mpia.de
†Member of the International Max Planck Research School for Astronomy, and Cosmic Physics at the University of Heidelberg, IMPRS-HD, Germany.

© 2014 The Authors
Published by Oxford University Press on behalf of the Royal Astronomical Society.
star clusters and later expanded due their peculiar environmental-driven evolution; this hypothesis will be tested in this study. Evolutionary processes that are often assumed to cause an expansion are strong tidal shocks (Spitzer 1958; Ostriker, Spitzer & Chevallier 1972) or accretion process on to the MW halo (Mackey & Gilmore 2004; Miholics, Webb & Sills 2014). The latter mechanism assumes that these clusters formed in dwarf-like satellite galaxies that later were stripped and accreted on to the halo of the host galaxy. We note that accretion of dwarf galaxies is a process commonly used to explain the structural properties of GC systems. In fact, there is growing evidence that a significant fraction of MW GCs are accreted systems, while the remaining formed in situ in the early phase of galaxy formation (Marín-Franch et al. 2009; Forbes & Bridges 2010; Leaman, VandenBerg & Mendel 2013). This is further supported by the spatial coincidence of outer halo GCs with stellar streams and overdensities (Mackey et al. 2010).

In this work, we focus on the possibility that extended clusters formed in the context of an accretion event, testing if their observed extended sizes can be explained by the structural adjustment of the clusters to the time-dependent tidal field. We evaluate this hypothesis using N-body simulations considering the case of a cluster formed in the central regions of dwarf-like galaxies, where it experiences a compressive tidal field, which is then switched off to mimic the accretion of the cluster on to a MW-like galaxy. Compressive tides provide an extreme environment that enables the cluster to acquire an excess of kinetic energy with respect to its potential energy. A complementary approach has been followed by Webb et al. (2014) and Miholics et al. (2014) for the study of the evolution of the size of clusters embedded in less extreme (non-tidally compressive) environments.

The Letter is organized as follows: first, we introduce the compressive tidal environment typical of cored regions of galaxies and show with analytical calculations that an accretion event causes an expansion of stellar systems. Then, in Section 3, we present our N-body simulations and we discuss our results. Finally, we report our conclusions in Section 4.

### 2 EXPANSION OF CLUSTERS DUE TO SATELLITE ACCRETION

#### 2.1 Compressive tides in galaxy cores

Let us consider a gravitational potential $\phi$ embedding a star cluster. The associated tidal tensor can be written as the second space derivative of the potential (Renaud et al. 2008)

$$T^{ij} = -\partial^i \partial^j \phi.$$  (1)

The tides are fully compressive if all eigenvalues $\lambda$, of this tensor are negative, and extensive if at least one eigenvalue is positive. One typical environment of compressive tides is the central region of galaxies with cored density profiles. For dwarf galaxies, recent studies show that cored profiles are favoured over cuspy ones (e.g. Walker & Peharrubia 2011). In the case of a Plummer potential with characteristic radius $r_0$, fully compressive tides are found in the central region, delimited by $r < r_0/\sqrt{2}$ (Renaud 2010).

#### 2.2 Proof of the principle

We wish to describe the expansion of a stellar system due to a time-varying tidal field. We consider a GC initially embedded in an isotropic compressive tidal field that is then instantaneously removed (impulsive approximation; Spitzer 1958) to mimic the accretion event of the satellite that hosts the cluster in its centre. In this section, we follow the procedure outlined in Hills (1980).

Let us consider an isotropic tidal field such that the eigenvalues of the tidal tensor are equal, $\lambda = \lambda$, and negative (fully compressive tides). The initial energy of the cluster embedded in such field is (Renaud 2010, his equation E.12)

$$E_0 = \frac{1}{2} M_c \sigma^2 - \frac{G M^2}{2r_v} - \frac{1}{2} \lambda \alpha r_c^2,$$  (2)

where the last term describes the energy due to the compressive tides, $M_c$ the total mass of the cluster, $\sigma$ its velocity dispersion, $r_v$ the virial radius, $r_c$ the radius where the density of the cluster drops to zero, and $\alpha$ depends on the mass profile of the cluster and is defined as $\alpha = \frac{1}{G M_c} \int_0^{r_c} r^2 dm$. We assume that the system is virialized before the compressive tides are removed (Renaud 2010, his equation E.13)

$$M_c \sigma^2 - \frac{G M^2}{2r_v} + \lambda \alpha M_c r_c^2 = 0.$$  (3)

Since $\lambda$ is negative, we see that the velocity dispersion of the cluster is higher than what expected from a no-tide case.

In the impulsive approximation, we assume that both velocity dispersion and the radii of the cluster remain unchanged when the tidal field is instantaneously removed. This approximation is justified by the fact that the time-scale in which the stripping of a dwarf galaxy occurs is small compared to its internal dynamical time-scale. The new energy of the system is therefore

$$E_1 = \frac{1}{2} M_c \sigma^2 - \frac{G M^2}{2r_v},$$  (4)

and, by using equation (3), we get

$$E_1 = -\lambda \alpha M_c r_c^2 - \frac{1}{2} M_c \sigma^2.$$  (5)

The cluster remains bound ($E_1 < 0$) for

$$\lambda > \frac{1}{2} \frac{\sigma^2}{\alpha r_c^2}.$$  (6)

Therefore, if the system is embedded in too strong compressive tides (very negative values of $\lambda$), its energy exceeds the reference level which would allow it to remain bound after the impulsive change. The cluster is then ‘supervirialized’ and is unbound when the tides are switched off. We here consider unbound when the total energy is positive, in reality the core can remain bound and stars in the outer part escape with velocities larger than the escape velocity.

After turning off the tidal field, the cluster settles in a new equilibrium state on a dynamical time-scale, with a new radius $r_v$, and a new velocity dispersion $\sigma'$. Neglecting any mass-loss (i.e. constant $M_c$ over a dynamical time), the final state is described by the virial equation

$$M_c \sigma'^2 - \frac{G M^2}{2r_v'} = 0,$$  (7)

and a total energy

$$E = -\frac{G M^2}{4r_v'}.$$  (8)

Using equations (3), (4), and (8) we obtain a relation between the virial radius $r_v'$ at the final state and the initial radius $r_v$

$$r_v' = r_v \left(1 + \frac{2 \lambda \alpha r_c^2}{G M_c}\right)^{-1}.$$  (9)
In the case of compressive tides (i.e. $\lambda < 0$), the final virial radius $r_{v}^\prime$ is always larger than the initial $r_{v}$. The cluster therefore expands after the tidal field has been switched off.

In a realistic case, we would expect that the expansion would affect more the stars in the outer part of the cluster. These stars will escape with non-zero velocities, taking away a large fraction of the energy gained during the compressive phase. This could indeed reduce the expansion. Therefore, we discuss more detailed simulations in the next section.

3 N-BODY SIMULATIONS

We now study the problem with N-body simulations, using $\text{NBody6TT}$ (Renaud et al. 2011) based on $\text{NBody6}$ (Aarseth 2003). $\text{NBody6TT}$ gives the possibility to add to the regular forces the effect of an arbitrary time-dependent tidal field. We use the graphics processing unit (GPU) enabled version of Nitadori & Aarseth (2012) and compute the simulations using the GPU cluster at the University of Surrey.

Our fiducial initial conditions for the cluster consist of 4096 particles drawn from a Plummer sphere. Since our investigation focuses specifically on the effects of an abrupt variation of the tidal environment of the star cluster, we consider exclusively equal-mass models, in the absence of stellar evolution. The compressive tides are given by the central region of another Plummer potential, mimicking the cored potential well in the centre of a dwarf galaxy (see Section 2.1). The tidal tensor is computed analytically and fed to $\text{NBody6TT}$. The tides are switched off to simulate the stripping of the dwarf galaxy as a consequence of the accretion process on to the MW. For simplicity, the potential of the MW is not considered: the clusters experience the tides from the dwarf galaxy alone, which are then fully removed.$^3$

In the following sections, we present the results of the long-term dynamical evolution of the cluster, considering different initial densities, tidal field strengths, transitions between compressive tides and isolation (impulsive or adiabatic transitions), and in orbit inside the dwarf galaxy potential. We consider as bound stars those with $E < 0$ (Renaud et al. 2011), where the energy is given by the sum of the potential and kinetic energy, $E=U+K$.

3.1 Evolution in the centre of a compressive tidal potential

The first case we explore consists in a cluster with virial radius $r_{v} = 1$ pc. We aim to study the dependence of the cluster’s evolution on the strength of the tidal field. For this reason, we place the cluster with no orbital motion in the centre of a dwarf galaxy with total mass $M = 10^{8} M_{\odot}$ and scale radius $r_{s} = 1000, 500, 100$ pc (typical values for dwarf galaxies masses and characteristic radii; McNamachie 2012). The tidal field experienced is thus compressive, constant, and isotropic. We label these three compressive tidal fields as weak, intermediate, and strong. The compressive tides are switched off at 8 Gyr. At this time, the clusters have already undergone core collapse and have expanded to their maximum extent (see Fig. 1).

$^3$ We note that our low- $N$ cluster evolves to lower densities than real clusters. This is because in the expansion phase clusters evolve to a constant ratio of relaxation time over age, such that the clusters density is proportional to $N^2$. From equation (9), we see that the expansion factor is smaller for cluster with higher density. This means that more massive clusters are less affected by the removal of the tides than the clusters in our N-body models.

![Figure 1. Time evolution of the Lagrangian radii (enclosing 10, 50, and 90 per cent of the total bound mass) of a cluster in three compressive tidal fields, labelled as weak (green lines), intermediate (orange lines), and strong (blue lines) tidal field. When the compressive tides are switched off at 8 Gyr (vertical line), the cluster expands. However, the expansion is not enough to generate objects more extended than the one evolved in isolation (black lines).](https://example.com/figure1.png)

In Fig. 1, we show the time evolution of the 10, 50, and 90 per cent Lagrangian radii of the cluster (i.e. the radii containing 10, 50, and 90 per cent of the bound mass, respectively) for the strong, intermediate, and weak compressive tidal fields. The evolution of the tidally perturbed model is compared to the one of an isolated cluster. While the compressive tides are present, the spatial extent of the cluster depends on the strength of the tidal field: the stronger the field, the more compact the cluster is. The initial setup of the clusters ensures equipartition between kinetic and internal potential energies, and neglects the tidal term ($K/W = -0.5$). During the first phase, the negative energy brought by the compressive tides is balanced by an excess of kinetic energy with respect to the sole internal potential ($K/W < -0.5$). The time evolution of the ratio $K/W$ is depicted in Fig. 2.

When the compressive tidal field is switched off (8 Gyr), the cluster experiences an expansion, that is larger for stronger tides. We note that the expansion is significant for the 50 and 90 per cent Lagrangian radii, while is negligible for the inner 10 per cent Lagrangian radius, confirming that tides only affect the outer regions of clusters. We compare the spatial structure of the clusters evolved in compressive tides with the corresponding clusters evolved in isolation. From Fig. 1, it is clear that the expansion due to the abrupt variation of the tidal environment fails to produce objects that are more extended than the isolated cluster. We test this conclusion using a wide range of initial conditions including different initial cluster densities (initial virial radius of $r_{v} = 0.4, 1, 2.5$ pc, initial number of particles $N = 4096, 8192$) and circular orbits for the cluster inside the compressive tidal region. None the less, all star clusters that underwent such a process are always less extended than the one evolved in isolation (a summary of the runs is reported in Table 1).

3.2 Impulsive versus adiabatic tidal change

So far, we considered the case of an impulsive transition between the regime of compressive tidal field and no tidal field. We explore the effect of an adiabatic transition, occurring over a
The formation of extended start clusters

The clusters are initialized with $K/W = -0.5$, i.e. neglecting the tides, but subsequently adjust quickly to it (see especially the case with strong tides). When compressive tides are switched off, the cluster is in a ‘supervirialized’ state and tends to retrieve a virialized one by expanding. The peaks correspond to the formation of binaries.

Table 1. Ratios, $R_{10,50,90}$, of the 10, 50, and 90 per cent Lagrangian radii at 10 Gyr of a cluster evolved in compressive tides and then released to isolation at 8 Gyr and the corresponding one evolved in isolation. The names of the simulations indicate the strength of the compressive tidal field (W, I, S, for weak, intermediate, or strong; see Section 3.1) or a circular orbit at 250 pc from the dwarf galaxy centre, indicated with C. The initial number of particles $N$ and virial radius $r_v$ are reported. For I_4k_ad, the transition between the regime of compressive tides and isolation is adiabatic (see Section 3.2). Clusters evolved in compressive tides are always less extended than the one evolved in isolation.

| Model     | $N$  | $r_v$ | $R_{10}$ | $R_{50}$ | $R_{90}$ |
|-----------|------|-------|----------|----------|----------|
| W_4k      | 4096 | 1 pc  | 0.53     | 0.75     | 0.80     |
| I_4k      | 4096 | 1 pc  | 0.68     | 0.74     | 0.76     |
| S_4k      | 4096 | 1 pc  | 0.40     | 0.46     | 0.56     |
| I_8k      | 8192 | 1 pc  | 1.01     | 0.90     | 0.83     |
| C_4k      | 4096 | 0.4 pc| 1.01     | 0.65     | 0.52     |
| C_4k_1    | 4096 | 1 pc  | 0.92     | 0.77     | 0.69     |
| C_4k_2    | 4096 | 2.5 pc| 0.66     | 0.60     | 0.84     |
| I_4k_ad   | 4096 | 1 pc  | 0.63     | 0.72     | 0.72     |

3.3 Observational surface density and velocity dispersion profiles

A further confirmation of the inefficiency of satellite accretion events in forming extended stellar systems, is given by the detailed

![Figure 3](https://example.com/figure3.png) Time evolution of the 90 per cent Lagrangian radius for a simulation with an impulsive transition between compressive tidal field and isolation (orange line) and one with an adiabatic transition lasting 600 Myr (cyan line). An intermediate strength of the compressive tidal field is used (see Fig. 1) and the corresponding eigenvalues $\lambda$ are shown in the lower sub-panel. The 90 per cent Lagrangian radii converge in short time to the same value.

![Figure 4](https://example.com/figure4.png) Surface density profile (top panel) and line-of-sight velocity dispersion profile (bottom panel) at 10 Gyr of a cluster evolved in isolation (black line) and one evolved in intermediate-strength compressive tides (orange line) and released to isolation at $t = 8$ Gyr. No significant structural differences are observable.

The profiles are constructed by stacking three snapshots around 10 Gyr, assuring to have a number of stars $>100$ per radial bin.

Note that the number of particles of the two clusters at 10 Gyr is comparable ($N_{\text{isolated}} = 1619$ and $N_{\text{tides}} = 1413$) and the measured half-mass radii are $r_m = 11.49$ and 8.16 pc, for isolated and compressive tides case, respectively.

Footnotes:
2 This time-scale is the other extreme (compared to the impulsive transition), lasting longer than a typical accretion event.

3 The profiles are constructed by stacking three snapshots around 10 Gyr, assuring to have a number of stars $>100$ per radial bin.

4 Note that the number of particles of the two clusters at 10 Gyr is comparable ($N_{\text{isolated}} = 1619$ and $N_{\text{tides}} = 1413$) and the measured half-mass radii are $r_m = 11.49$ and 8.16 pc, for isolated and compressive tides case, respectively.
4 CONCLUSIONS

We tested the possibility that extended clusters form originally in the dense central regions of dwarf galaxies and later expand due to a time-variation of the tidal field induced by the accretion of the host dwarf galaxy. In the core regions of dwarf galaxies, the clusters experience a regime of compressive tides that produces an excess of kinetic energy with respect to the internal potential energy. When the dwarf galaxy is accreted on to the MW, the clusters are released in the outer halo and expand due to this excess of energy.

We find that the expansion imprinted to the clusters does not give origin to objects that are more spatially extended than systems that have always evolved in isolation. We tested our conclusion exploring different initial densities for the clusters, orbits inside the core of the dwarf galaxy, strengths of the compressive tides and time variations of the transition from the regime of compressive tides to isolation.

We note here that our result can be considered as conservative. In fact, we tested the most extreme case in which the cluster originally resides in the central compressive region of a dwarf galaxy and is then released in isolation due to the accretion event. In a more realistic case, the accretion process of the dwarf galaxy would bring the cluster in the (extensive) tidal potential of the host galaxy. This would set a natural boundary for the spatial extent of the cluster (Lagrange surface), that would further limit its expansion. Moreover, by setting compressive tides, we push further the results of Miholics et al. (2014) who found that the (less extreme) case of tidally extensive tides does not lead to accreted clusters more extended than those in isolation.

We conclude that an accreted origin of outer halo extended clusters is unlikely to explain their large spatial extent. For this reason, these stellar systems could have genuinely formed extended or could have experienced an enhanced expansion due to some internal dynamical mechanism (e.g. the interplay of primordial mass segregation and dynamical relaxation; Haghi et al. 2014). Alternatively, observations of the radius of extended clusters could be biased by unbound stars that have already been stripped, and wonder in its vicinity along its orbit (Küpper et al. 2010).

ACKNOWLEDGEMENTS

This work was carried out as part of the ISIMA programme on Gravitational Dynamics held in 2014 July at CITA, Toronto. We acknowledge Pascale Garaud for the organization, the financial support, and for the stimulating environment provided by all the participants. PB acknowledges support from Heidelberg Graduate School for Fundamental Physics, FR acknowledges support from the European Research Council (ERC) through grant ERC-StG-257720.

MG acknowledges financial support from the Royal Society in the form of a University Research Fellowship (URF) and an equipment grant used for the GPU cluster in Surrey. MG and FR acknowledge support from the ERC (ERC-StG-335936, CLUSTERS) and ALV from RCE1851. Finally, all authors thank Sverre Aarseth and Keigo Nitadori for making the GPU version of NBODY6 available, and Dave Munro for the hardware support at the University of Surrey.

REFERENCES

Aarseth S. J., 2003, Gravitational N-Body Simulations. Cambridge Univ. Press, Cambridge
Assmann P., Wilkinson M. I., Fellhauer M., Smith R., 2011, MNRAS, 413, 2606
Belokurov V., Irwin M. J., Koposov S. E., Evans N. W., Gonzalez-Solares E., Metcalfe N., Shanks T., 2014, MNRAS, 444, 2124
Brodie J. P., Larsen S. S., 2002, AJ, 124, 1410
Elmegreen B. G., 2008, ApJ, 672, 1006
Fellhauer M., Kroupa P., 2002, AJ, 124, 2006
Forbes D. A., Bridges T., 2010, MNRAS, 404, 1203
Frank M. J., Grebel E. K., Küpper A. H. W., 2014, MNRAS, 443, 815
Gieles M., Heggie D. C., Zhao H., 2011, MNRAS, 413, 2509
Haghi H., Hoseini-Rad S. M., Zonoozi A. H., Küpper A. H. W., 2014, MNRAS, 444, 3699
Harriss W. E., 2010, preprint (arXiv:1012.3224)
Hills J. G., 1980, ApJ, 235, 986
Huxor A. P. et al., 2014, MNRAS, 442, 2165
Küpper A. H. W., Kroupa P., Baumgardt H., Heggie D. C., 2010, MNRAS, 407, 2241
Leaman R., VandenBerg D. A., Mendel J. T., 2013, MNRAS, 436, 122
McConnachie A. W., 2012, AJ, 144, 4
Mackey A. D., Gilmore G. F., 2004, MNRAS, 355, 504
Mackey A. D., van den Bergh S., 2005, MNRAS, 360, 631
Mackey A. D. et al., 2010, ApJ, 717, L11
Mackey A. D. et al., 2013, ApJ, 770, L17
Marín-Franch A. et al., 2009, ApJ, 694, 1498
Miholics M., Webb J. J., Sills A., 2014, MNRAS, 445, 2872
Nitadori K., Aarseth S. J., 2012, MNRAS, 424, 545
Ostriker J. P., Spitzer L., Jr, Chevalier R. A., 1972, ApJ, 176, L51
Renaud F., 2010, PhD thesis, Universitè Wien, Université de Strasbourg
Renaud F., Boily C. M., Fleck J.-J., Naab T., Theis C., 2008, MNRAS, 391, L98
Renaud F., Gieles M., Boily C. M., 2011, MNRAS, 418, 759
Spitzer L., Jr, 1958, ApJ, 127, 17
Walker M. G., Peñarrubia J., 2011, ApJ, 742, 20
Webb J. J., Leigh N., Sills A., Harris W. E., Hurley J. R., 2014, MNRAS, 442, 1569

This paper has been typeset from a T/X/LX/X file prepared by the author.