Study of Azimuthal Correlations in the Target Fragmentation Region in p, d, He, C + C, Ta and C+Ne, Cu Collisions at a Momentum of 4.2, 4.5 and 10 AGeV/c

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Abstract. Azimuthal correlations between the same type of particles (protons or pions) in the target fragmentation region was studied in d, He, C + C, Ta (4.2 AGeV/c), C + Ne, Cu (4.5AGeV/c) and p + C, Ta (10 GeV/c) interactions. The data were obtained from the SKM-200-GIBS streamer chamber and from Propane Bubble Chamber (PBL-500) systems utilized at JINR. Study of multiparticle azimuthal correlations offers unique information about space-time evolution of the interactions. Azimuthal correlations were investigated by using correlation function $C(\Delta \phi) = dN/d(\Delta \phi)$, where $\Delta \phi$ represents the angle between the sums of transverse momenta vectors for particles emitted in the forward and backward hemispheres. For protons a "back-to-back" ("negative") azimuthal correlations were observed in the above mentioned interactions. The absolute values of the correlation coefficient $|\xi|$ – the slope parameter of $C(\Delta \phi)$, strongly depend on the mass number of the target ($A_T$) nuclei in the nucleon-nucleus and nucleus-nucleus collisions. Namely, $|\xi|$ – decreases with increase of $A_T$ in p+C and p+Ta collisions, while $|\xi|$ decreases from d+C up to C+Ne and then almost does not change with increase of $A_T$ in p+C and p+Ta collisions. For pions a "back-to-back" correlations were obtained for a light targets (C, Ne), and a "side-by-side" ("positive") correlations for a heavy targets (Cu, Ta). The $|\xi|$ insignificantly changes with increase of the momenta per nucleon and almost does not change with increase of $A_P$ and $A_T$. Models, used for description of the data – the Ultra relativistic Quantum Molecular Dynamic (UrQMD) and Quark-Gluon String Model (QGSM), satisfactorily describe the obtained experimental results.

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1 Introduction

Studies of multi-particle correlations have provided crucial insight into the underlying mechanism of particle production in relativistic heavy-ion collisions. The primary goal of current relativistic heavy ion research is the creation and study of nuclear matter at high energy densities [1, 2]. Open questions the detailed properties of such excited matter, as well as a transition to the quark-gluon plasma (QGP) phase. Such a phase of deconfined quarks and gluons has been predicted to survive for $\sim 3-10$ fm/c in Au-Au collisions at the Relativistic Heavy Ion Collider (RHIC) [3] and several experimental probes have been proposed for its possible detection and study [4]. The most prominent feature of multi-particle correlations in AA collisions is due to collective flow [5,6], an azimuthal anisotropy in momentum space induced by strong expansion of the initial almond-shaped overlap area of two nuclei [5]. Collective flow constitutes an important observable [7] because it is thought to be driven by pressure built up early in the collision, and therefore can reflect conditions exciting in the first few fm/c. Collective flow leads to an anisotropy in the azimuthal distribution of emitted particles. Studies of elliptic flow have been carried out over a wide range of energies and systems at both RHIC and the LHC [8–12]. Study of multiparticle azimuthal correlations offers unique information about space-time evolution of the collective systems [13,14]. One of the interesting methods proposed in [15–16] is the conventional division of phase space into forward and backward moving particles according to the rapidity and emission angle or into slow and fast particles according to energy.

During last years we have analyzed our experimental data following the method [17,18]. The collective vari-
ables and their dependencies on the transverse momentum of all secondary charged particles in the azimuthal plane, were studied to reveal a nontrivial effects in nucleus-nucleus collisions [17–21]. We have investigated multiparticle azimuthal correlations of protons and pions in central and minimal bias inelastic collisions (4.2, 4.5 and 10 GeV/c/nucleon) within two experimental setups – 2 m streamer chamber placed in a magnetic field (SKM-200-GIBS) and 2 m Propane Bubble Chamber (PBC-500) of JINR. In order to investigate the mechanism of nucleus-nucleus interactions we have studied the correlations of these particles (protons, pions, A-hyperons) with respect to the reaction plane (directed and elliptic flows) [17–19], as well as with respect to the opening angle between particles emitted in the forward and backward hemispheres [20,21].

In this paper, we present results of the analysis of azimuthal multiparticle correlations in the target fragmentation region in d, He, C + C, Ta (4.2 A GeV/c), C + Ne, Cu (4.5 A GeV/c) and p + C, Ta (10 GeV/c) collisions between the same type of particles (protons or pions). The dependence of the azimuthal correlation coefficient on the mass numbers of projectile (A_P) and target (A_T) have been investigated.

2 Experimental data

The data were obtained from the SKM-200-GIBS streamer chamber and from the Propane Bubble Chamber systems (PBC-500) utilized at JINR. The SKM-200-GIBS setup is based on a 2 m streamer chamber placed in the magnetic field of 0.8 T and on a triggering system. C+Ne and C+Cu central collisions were studied only at the momentum of 4.5 A GeV/c, because the multiplicity of the second particles significantly increases using a central trigger. A central trigger selected events with no charged projectile spectator fragments at p < 3 GeV/c, within a cone of half angle of either 0.3° or 0.5°, depending on the run. The thickness of Cu solid target, in the form of a thin disc, was 0.2 g/cm². Neon gas filling of the chamber [22] also served as a nuclear target. Details of the acquisition techniques of 723 C+Ne and 663 C+Cu interaction data, and other experimental procedures have been presented in [22,23].

The 2 meter Propane Bubble Chamber (PBC-500) was placed in the magnetic field of 1.5 T. The procedures for separating out the p+C, d+C, He+C and C+C collisions in propane (C₂H₈) and the processing of the data including particle identification and corrections have been described in detail in Refs. [23,24]. The analysis produced 16509 p+C, 4581 d+C, 9737 He+C, 15962 C+C, 2342 p+Ta, 1424 d+Ta, 1532 He+Ta (at that d+Ta and He+Ta data were combined to increase statistics) and 2469 C+Ta inelastic collision events. The protons with momentum p<150 MeV/c were not detected within the PBC-500 (as far as their track lengths l < 2 mm) and protons with p < 200 MeV/c were absorbed in Ta target plate (the detector biases).

In the experiment, the projectile fragmentation products were identified as those characterized by the momentum p > 3.5 GeV/c (4.2, 4.5 A GeV/c) or p > 7 GeV/c (10 GeV/c) and polar angle Θ < 3.5° and the target fragmentation products – by the momentum p < 0.25 GeV/c in the target rest frame. After these selection criterions, the remaining protons were considered as the participant protons. For the analysis minimum three particles N_{particles} ≥ 3 in the event were required.

3 Azimuthal Correlations Between Protons or Pions

In Refs. [15,16] the method for studying the correlation between groups of particles has been developed. The azimuthal correlation function was defined [15,16] by the relative opening angle between the transverse momentum vector sums of particles emitted forward and backward with respect to the rest frame of the target nucleus (larger or smaller a rapidity of y_0=0.2). The method was used for analysis of the data at 4.9, 60 and 200 GeV (BEVALAC, CERN, CERN/SPS) [19]. We apply this method for our data. The analysis has been performed event by event. In each event, we denote the vectors:

\[ Q_B = \sum_{y_t < y_0} P_{\perp} \]

and

\[ Q_F = \sum_{y_t \geq y_0} P_{\perp} \]

where y_0 is 0.2 and y_t ≤ 1.33 for protons. This is guided by the experimental fact that the target rapidity distributions of protons peaks at y_0 ≈ 0.2 [27] and follows the idea of a target “fireball” moving with a rapidity y_0 (in the rest frame of the target nucleus). The influence of the actually chosen value of y_0 to the experimental results, furthermore, has been checked by varying y_0 in a reasonable range 0.1 ≤ y_0 ≤ 0.3 and within these limits no significant change of the correlation function has been observed. The correlation function C(Δφ) was determined as:

\[ C(\Delta\phi) = dN/d\Delta\phi, \]

where Δφ is the angle between the vectors Q_B and Q_F:

\[ \Delta\phi = \arccos \left( \frac{Q_B \cdot Q_F}{|Q_B| |Q_F|} \right). \]

Essentially, C(Δφ) measures whether the particles are preferentially emitted “back-to-back” or “side-by-side” correlations. “Back-to-back” means the “negative” correlations, where C(Δφ) increases with Δφ and reaches a maximum at Δφ = 180°. “Side-by-side” means the “positive” correlations, where C(Δφ) decreases with Δφ and have a maximum at Δφ = 0° [15,16].

In view of the strong coupling between the nucleons and pions, it is interesting to know the correlations between pions. Thus, we have studied correlations between
protons and between pions. Fig. 1–3 show the experimental correlation function \( C(\Delta \phi) \) for these particles in p, d, He, C + C, p, d, He, C + Ta and C + Ne, Cu collisions. One can observe from Figures a clear correlation for protons and for pions (the results obtained for better performance, specifically, the corresponding \( C(\Delta \phi) \) - distributions of protons are shifted below for C + Ne, Cu, Ta collisions by 0.85 factor). To quantify these experimental results, the data were fitted by the function:

\[
C(\Delta \phi) = a (1 + \xi \cos(\Delta \phi)),
\]

where \( a \) is a normalization constant.

Results of the fitting are listed in Table 1. The strength of the correlation is defined as:

\[
\zeta = C(0^\circ)/C(180^\circ) = (1 + \xi)/(1 - \xi).
\]

As it can be seen, the correlation coefficient \( \zeta < 0 \), and thus the strength of correlation \( \zeta < 1 \) for protons in all interactions. This means that protons are preferentially emitted back-to-back.

One can observe from Figs. 1 and 2, a clear back-to-back (\( \xi < 0, \zeta < 1 \)) correlations for pions in light systems p, d, He, C + C and C + Ne. For heavy, asymmetric pairs of p, (d+He), C + Ta and C + Cu the side-by-side (\( \xi > 0 \) and \( \zeta > 1 \)) correlations of pions can be seen from Fig. 3 (Table 1).

We have studied also a dependence of the correlation coefficient \( |\xi| \) on \( A_P, A_T \) for protons and pions. The absolute values of \( \xi \) for protons decreases with increase of \( A_T \) in the nucleon-nucleus collisions: 0.302±0.013 for p+C up to 0.143±0.027 for p+Ta (10 GeV/c). What concerns nucleus-nucleus collisions, \( |\xi| \) initially linearly decreases with increase of \( A_P, A_T \) from 0.296±0.022 (d+C) up to 0.150±0.030 (C+Ne), and then almost does not change with increase of \( A_P, A_T \). For pions, \( |\xi| \) insignificantly changes with increase of the momenta per nucleon and almost does not change with increase of \( A_P, A_T \): |\xi| = 0.107±0.019 for p+C and it’s almost the same for C+Ta (Table 1).

The obtained experimental results for p, d, He, C + C, Ta collisions have been compared to the predictions of the Ultra relativistic Quantum Molecular Dynamic (UrQMD) model \([25,29]\) coupled with the Statistical Multifragmentation (SMM) model \([30]\), and the Quark-Gluon String Model (QGSM) \([31,32]\) for C + C, Ne, Cu, Ta interactions.

The UrQMD model is a microscopic transport model based on the covariant propagation of all hadrons on classical trajectories in a combination with stochastic binary scatterings, colour string formation and resonance decay. The SMM model \([30]\) was added to the UrQMD model \([33,34]\) to improve simulations of a baryon production in target and projectile fragmentation regions. There is not a strong subdivision between the participating protons and protons created at the de-excitation of nuclear residuals. The SMM allows a simulation of the evaporated proton production, and UrQMD generates the participating protons. Thus, we have in the model events of all processes presented in the experiment. The UrQMD model is designed as a multi-purpose tool for studying a wide variety of heavy-ion-related effects ranging from multifragmentation and collective flow to particle productions and correlations in the energy range from SIS to RHIC.

The experimental selection criteria of events were applied to the events generated by the enlarged UrQMD model (UrQMD+SMM), 51191 (10 GeV/c) p+p, 27502 (4.2 A GeV/c) d+C, 31716 (4.2 A GeV/c) He+C, 35754 (4.2 A GeV/c) C+C, 7230 (10 GeV/c) p+Ta, 5137 (4.2 A GeV/c) d+Ta, 3210 (4.2 A GeV/c) He+Ta and 9130 (4.2 A GeV/c) C+Ta interactions have been chosen after the experimental events selection criteria. The values of the correlation coefficient \( \xi \) were extracted for protons and pions from corresponding distributions for each nuclear pair (Table 1). One can see, that there is a good agreement between the experimental and theoretical values (Figs. 1–4).

Detailed description of the QGSM can be found in \([31,32]\). This model is based on the Regge and string phenomenology of particle production in inelastic binary hadron collisions. Within QGSM, nuclear densities are used for selecting coordinates of original nucleons. This is followed by the formation of quark-gluon strings which fragment into hadrons. Those hadrons rescatter. In QGSM, the sole cause of sideward flow is the hadron rescattering. In all other models in the literature, where produced pressure comes from rescattering alone, the flow in the specific energy regime was found significantly underestimated, albeit predominantly in heavier systems \([35]\). However, in collisions studied here, QGSM turned out to describe the azimuthal correlations rather well (Figs. 2–4).

For simulating the model events, we have employed the COLLI Monte-Carlo generator \([36]\) based on QGSM. To the generated events, the trigger filter has been applied in the case of C + C, Ne, Cu, Ta interactions. In mimicking, in particular, the deterioration of experimental efficiency for registering vertical tracks, protons characterized by deep angles greater than 60° have been excluded from an analysis. For the present study, 36495 C+C, 16637 C+Ne, 8347 C+Cu and 9721 C+Ta collisions at a momentum of 4.2, 4.5 A GeV/c have been chosen to the analysis (Table 1). The mass dependence, as seen in Fig. 4 is, in particular, fairly well reproduced. C + C, Ne, Cu, Ta events have been generated at fixed b-values equal to: \( < b > = 2.65, 2.20, 2.75 \) and 6.54 (fm), respectively.

Finally, both models describe experimental results. As seen, there is a good agreement between the experimental and MC data. The experimental results from C+C and C+Ta collisions have been compared to the results obtained by the UrQMD and QGSM models in order to study the accuracy of the mechanism of nucleus-nucleus interactions implemented in these models. The values of the correlation coefficients in the experimental and MC data for protons and pions are in a good agreement for all studied systems.

Back-to-back correlations have been observed between protons with the Plastic-Ball detector in p + Au collisions at energy of 4.9, 60, 200 GeV/c and in (O, S)Au reactions at 200 GeV/c \([10,37]\). Because, the azimuthal correlation
function was defined in the target fragmentation region, the correlation parameters in the wide range of energy increases inappreciable. We applied this method also in our previous articles [20,21], where the analysis was carried out in the whole rapidity region instead of the target fragmentation region [15,16]. In the case, instead of $y_0$ – an average rapidity of participant protons for each colliding pears, $y_0$ was used.

The back-to-back emission of protons can be understood as results of (local) transverse momentum conservation [15]. Back-to-back ($\xi < 0$, $\zeta < 1$) pion correlation for light systems $p$, $d$, $He$, $C + C$ and $C + Ne$, and the side-by-side pion azimuthal correlations ($\zeta > 0$ and $\zeta > 1$) for heavy, asymmetric pairs $p$, $d$, $He$, $C + Ta$ and $C + Cu$, i.e. change of the pion’s azimuthal correlation type, are in agreement with our previous results [20,21]. Also, the side-by-side correlations of pions have been observed in $p+Au$ collisions at Bevalac (4.9 GeV/nucleon) and CERN-SPS (60 and 200 GeV/nucleon) energies [10]. Another investigations of large angle two-particle correlations, carried out at the 3.6 AGeV C-beam in Dubna [3], showed a back-to-back pion correlation for a light target (Al), and a side-by-side correlation for a heavy target (Pb). For protons a back-to-back correlation was observed for all targets. All above mentioned results appear to be consistent with our results of proton and pion azimuthal correlations and with the variation of the pion correlation when going from $(d+C)$ to $(C+Cu)$.

The reason for the observed difference between protons and pions is that the pions are absorbed in the excited target matter (π + N → ∆ and $∆ + N → N + N$) [15,16]. The side-by-side correlation of pions can be naturally explained on the base that pions, which are created in collision suffer at $b \neq 0$ fm ($b$ is the impact parameter) either rescattering or even complete absorption in the target spectator matter. Both processes will result in a relative depletion of pions in the geometrical direction of the target spectator matter and hence will cause an azimuthal side-by-side correlation as observed in the experimental data.

4 Conclusion

The study of multiparticle azimuthal correlations between protons or between pions in the target fragmentation region in $d$, $He$, $C + C$, $Ta$ (4.2 A GeV/c), $C + Ne$, $Cu$ (4.5 A GeV/c) and $p + C$, $Ta$ (10 GeV/c) collisions have been carried out. The $pC$ system is the lightest studied one, and the $pTa$ is extremely asymmetrical system in which azimuthal correlations between protons and between pions in the "backward" and "forward" hemispheres have been detected:

1. For protons a back-to-back correlation was observed for all interactions. The absolute values of $\xi$ for protons decreases with increase of the mass numbers of target $Ar$ nuclei in the nucleon-nucleus collisions: $0.392\pm0.013$ for $p+C$ up to $0.143\pm0.027$ for $p+Ta$ at 10GeV/c. What concerns nucleus-nucleus collisions, $|\xi|$ initially linearly decreases with increase of the mass number of projectile $A_P$ and target $A_T$ nuclei from 0.296±0.022 ($d+C$) up to 0.150±0.030 ($C+Ne$) and then almost does not change with increase of $A_P$, $A_T$.
2. As shown, the pions exhibit "back-to-back" (negative) correlations consistent with that for protons for light systems of $p$, $(d+He)$, $C + C$ and $C + Ne$ (light targets – $C$, $Ne$) and a side-by-side correlations for heavy, asymmetric pairs of $p$, $d$, $He$, $C + Ta$ and $C + Cu$ (heavy targets – $Cu$, $Ta$). The correlation coefficient (|$\xi$|) insignificantly changes with increase of the momenta per nucleon and almost does not change with increase $A_T$, $A_T$ nuclei: $|\xi| = 0.107\pm0.019$ for $p+Cu$, and it’s almost the same for $C+Ta$.
3. Both models, UrQMD and QGSM satisfactorily describe the experimental results, there is a good agreement between the experimental and theoretical values.

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Figure and Table captions

Fig. 1. The dependence of the correlation function $C(\Delta\phi)$ on the $\Delta\phi$ for protons and pions in experimental (●, ▲) and UrQMD (○, △) (pC, dC, HeC, CC), QGSM (∗, ⋆) (CC) MC data, respectively. The curves are the results of the approximation of the data (see text).

Fig. 2. The dependence of the correlation function $C(\Delta\phi)$ on the $\Delta\phi$ from CNe collisions for protons and pions in experimental (●, ▲) and QGSM (∗, ⋆) MC data, respectively. The curves are the results of the approximation of the data (see text).

Fig. 3. The dependence of the correlation function $C(\Delta\phi)$ on the $\Delta\phi$ for protons and pions in experimental (●, ▲) and UrQMD (○, △) (p, d+He)Ta, (CTa), QGSM (∗, ⋆) (CCu, CTa) MC data, respectively. The curves are the results of the approximation of the data (see text).

Fig. 4. The dependence of $|\xi|$ correlation coefficient on $(A_P + A_T)^{1/2}$ for protons (upper points) and pions (lower points) in pC, dC, HeC, CC, pTa, CNe, (dHe)Ta, CCu and CTa collisions. Closed symbols correspond to experimental (●, ▲), and open ones to the UrQMD (○, △), stars to the QGSM (∗, ⋆) MC data, respectively.

Table 1. The number of experimental and Monte-Carlo (MC) generated (UrQMD and QGSM) events ($N_{\text{event}}$), the correlation coefficient ($\xi$) for protons and pions in these collisions.
Table 1.

| $A_p$, $A_T$ | $N_{events}$ | $\xi_{prot}$ | $\xi_{pion}$ | $\sqrt{A_p} \times A_T$ |
|--------------|-------------|--------------|--------------|---------------------------|
| pC           | $exp.$ 16509 | $-0.302 \pm 0.013$ | $-0.107 \pm 0.019$ | 3.50                      |
|              | UrQMD 50191 | $-0.298 \pm 0.012$ | $-0.112 \pm 0.012$ |
| dC           | $exp.$ 4581  | $-0.296 \pm 0.022$ | $-0.108 \pm 0.028$ | 4.93                      |
|              | UrQMD 27502 | $-0.306 \pm 0.009$ | $-0.104 \pm 0.010$ |
| HeC          | $exp.$ 9737  | $-0.259 \pm 0.021$ | $-0.103 \pm 0.018$ | 6.93                      |
|              | UrQMD 31716 | $-0.252 \pm 0.016$ | $-0.109 \pm 0.012$ |
| CC           | $exp.$ 15962 | $-0.163 \pm 0.010$ | $-0.075 \pm 0.011$ | 12.00                     |
|              | UrQMD 35754 | $-0.161 \pm 0.014$ | $-0.076 \pm 0.012$ |
|              | QGSM 36495  | $-0.174 \pm 0.009$ | $-0.080 \pm 0.010$ |
| pTa          | $exp.$ 2342  | $-0.143 \pm 0.027$ | $0.111 \pm 0.021$  | 13.50                     |
|              | UrQMD 7230  | $-0.140 \pm 0.014$ | $0.116 \pm 0.015$  |
| CNe          | $exp.$ 723   | $-0.150 \pm 0.030$ | $-0.081 \pm 0.015$ | 16.60                     |
|              | QGSM 16637  | $-0.147 \pm 0.018$ | $-0.088 \pm 0.014$ |
| (d+He)Ta     | $exp.$ 2956  | $-0.153 \pm 0.022$ | $0.086 \pm 0.024$  | 23.00                     |
|              | UrQMD 17629 | $-0.148 \pm 0.012$ | $0.085 \pm 0.014$  |
| CCu          | $exp.$ 663   | $-0.139 \pm 0.035$ | $0.093 \pm 0.022$  | 27.70                     |
|              | QGSM 8347   | $-0.148 \pm 0.015$ | $0.082 \pm 0.017$  |
| CTe          | $exp.$ 2469  | $-0.144 \pm 0.025$ | $0.108 \pm 0.022$  | 46.60                     |
|              | UrQMD 9130  | $-0.148 \pm 0.014$ | $0.105 \pm 0.016$  |
|              | QGSM 9721   | $-0.160 \pm 0.006$ | $0.093 \pm 0.006$  |
Fig. 1.
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