Structural Transitions of Silicate Nanocrystals in the Glass

G. Abdurakhmanov*, G. S. Vakhidova

Institute of Power Engineering and Automation, the Uzbek Academy of Sciences, 29 Do‘rmon yo‘li, Tashkent, 100125 Uzbekistan

Abstract  The temperature dependences of resistivity and thermopower measurements reveal that nanocrystals of silicates in lead-silicate glass of various compositions undergo structural transitions in the temperature range of 800 – 1000 K. The diameter of these nanocrystals estimated from Scherrer’s formula is about 0.8 – 1.6 nm and each nanocrystal consists of 8 - 64 unit cells. Structure transitions are detected as sharply maxima of resistivity $\rho$ and thermopower $S$ at temperature $T = 800 – 100$ K. Lead-silicate glass was doped by RuO$_2$ up to 16 weight% to facilitate the measurements of the $\rho$ and the $S$. The doped lead-silicate glass has a metal-like behavior at the room temperature: the temperature dependences $\rho(T)$ and $S(T)$ are very slow, the value of the $S$ is typical for metals (few and tens of $\mu$V/K). Beyond the maximum of the resistance (temperature $T > 1000$ K) doped lead-silicate glass turns into typical semiconductor having energy gap about 0.05 – 1.5 eV depending on the composition of the glass. Anomalous thermal expansion of the RuO$_2$ relict crystals is detected at the temperatures of 800 – 1000 K as well.

Keywords structure transitions in nanocrystals, silicate glass, thermopower, resistivity, doping, thermal expansion

1. Introduction

Structural transitions as a fundamental property of interacting atoms in the crystalline state are very important for basic knowledge and applications. These transitions are collective phenomenon and therefore should depend on the number of atoms in the sample, i.e. on the size of the latter one. For example, the Curie temperature $T_C$ for nanostructured ferroelectrics decreases with the size $d$ of nanocrystals as $d^{-1}$, with it’s lowest value reaching $T_C \approx 300$ K at $d \approx 3$ nm (fig. 3 in [1]). The size of nanocrystals in these investigations was defined as the diameter of nanowire, i.e. in two directions only, while in the third direction (along the wire) the value of this parameter might be significantly higher.

Structural transitions in nanocrystals of LaMnO$_3$, having average dimensions about 15 - 20 nm, were investigated in [2]. It was found that transition temperature $T_C$ in these nanocrystals undergoes a reduction up to $T_C=493\pm10$ K in compared to $T_C=750$ K in the bulk samples.

To our knowledge, there is no information about structural transitions in smaller nanocrystals and in the nanocrystals formed in the glass.

All the silicate glasses have been devitrificated in time (tens or hundreds of years) so one can assume that nanocrystals of silica and various silicates are formed naturally in silicate glasses and structural transformations should take place in them. Dimensions of these nanocrystals are 1 – 2 nm as follows from X-ray diffraction patterns (Scherrer’s formula). For example, the structural transition of $\beta$-quartz into $\alpha$-quartz and vice versa takes place at 846 K and is accompanied by the increase of the unit cell volume by about 6 %[3]. Increase of interatomic distances due to the structural transitions leads to decrease in the electrical conductivity of the sample, so this effect can be exploited for collecting the information about the structural transitions. The unit cell of the $\beta$-quartz is trigonal with $a = 0.4893$ nm, $c = 0.5384$ nm at the room temperature, while the $\alpha$-quartz is hexagonal with $a = 0.4983$ nm, $c = 0.5419$ nm at 848 K.

Direct and doubtless evidences of existence of nanocrystals in the glass have not been thoroughly investigated before. That is why the problem of the glass structure (continuous random network, Zachariasen, 1932; microcrystallits, separated by interlayer of disordered atoms, Lebedev, 1921) is still the subject of discussions. But the temperature dependence of some glass properties such as viscosity, thermal expansion coefficient, dielectric constant and dielectric loss, have anomalies which have a better agreement with microcrystalline theory. This is especially the case of many-component glasses.

Here we show that structural transitions take place in nanocrystals of the average size of 1 – 2 nm in doped lead-silicate glass and are accompanied by sharp increase of the resistivity $\rho$ and the Seebeck coefficient $S$ at the temperatures below 1123 K. We found that at these temperatures the value of $\rho$ is 2 – 6 times higher than that value at room
temperature and $S$ may be as high as $10^3$ $\mu$V/K. Both $\rho$ and $S$ are affected by chemical composition of the glass.

Direct investigations of the structure of nanocrystals smaller than $3 - 4$ nm by diffraction methods (X-ray or neutron) are problematic, so one is forced to probe them by the indirect methods such as the measurements of the electrical properties (conductivity and thermopower). For example, structure transformations in ferroelectrics leads to sharp increase of resistivity $\rho$ and decrease of permittivity $\varepsilon$ as the interatomic distances increase[4].

2. Experiment

The samples of glass were doped by RuO$_2$ to reduce the resistivity and to enhance the thermopower in our experiments, so it is possible to measure the reduced value of resistivity of about $10^2 - 10^5$ Ohm-cm more accurately than that of the glass (about $10^{15} - 10^{16}$ Ohm-cm). The doping process used here is standard for technology of thick film resistors and was described elsewhere[5] (the mixture of the glass and the dopant powders have been fired at $T_f = 1125$ K in $t = 10$ min). Content of RuO$_2$ in our samples of doped glass was 16, 20 and 30 weight %. The lead-silicate glasses investigated have the following composition (weight %):

Glass1  SiO$_2$ – 33; PbO – 67;
Glass2  SiO$_2$ – 27; PbO – 67; BaO – 4; MgO – 2.

The mixture of oxides have been melted at temperatures $1723\pm20$ K (glass1) and $1623\pm20$ K (glass2) for 1 h. Density of the glasses by hydrostatic weighing is 4.81$\pm$0.02 g·cm$^{-3}$ for the glass1 and 5.13$\pm$0.02 g·cm$^{-3}$ for the glass2. The glass transition temperature $T_g$ have been evaluated by thermomechanical analysis (TMA, temperature dependence of the thermal expansion coefficient) and was found to be $760\pm20$ K for the glass1 and $785\pm20$ K for the glass2.

Samples of the doped glass for electrical measurements were the bulk material: 5 mm in diameter and 10 mm in height with the Pt or Ag electrodes. Samples for X-ray investigations were powders. The Pt heater of the D500 Siemens X-ray diffractometer was coated by these powders in the nitrocellulose lacquer. In the final X-ray patterns the diffraction lines of Pt have been deleted.

The values of resistance and thermopower were measured by digital multimeter Sch-300 having error less than 0.2%. The temperature was measured by the same multimeter and standard Pt-PtRh thermocouple. The thermocouple was calibrated in standard temperature points of water boiling (373 K), tin and silver solidification (505 and 1234 K accordingly).

Accuracy of determining of the lattice parameters of RuO$_2$ was about $\pm0.01$ Å and estimated from Bregg’s formula[6] for interplane distance $d = \lambda / 2 \sin \theta$ as

$$\Delta d / d = \Delta \lambda / \lambda + \Delta \theta \cos \theta / \sin \theta,$$  

(1)

here wavelength $\lambda = 0.15418$ $\pm 0.00001$ nm for CuK$_\alpha$ radiation, $\theta$ is the diffraction angle, $\Delta d$, $\Delta \lambda$ and $\Delta \theta$ are absolute errors of corresponding values. The crystallographic planes [002] and [220] of RuO$_2$ (rutile structure, tetragonal system) appear at $2\theta = 59.5$ and 58.1 accordingly in our experiments. The accuracy of the $2\theta$ is about 0.05 for Siemens D500 diffractometer so $d_{(002)} = 1.554 \pm 0.002$ Å and $d_{(220)} = 1.588 \pm 0.002$ Å. The according values of the lattice parameters are $c = 2d_{(002)} = 3.108 \pm 0.004$ Å and $a = 2\sqrt{d_{(220)}} = 3.176 \pm 0.006$ Å.

The mean size $L$ of the nanocrystals in the glass was estimated for the main halo at about $2\theta = 30 - 35^\circ$ via Scherrer’s formula[6] $L = \lambda / (B \cos \theta)$, where $K$ is the dimensionless shape factor (about 0.9) and $B$ is the line broadening at half maximum intensity (in radians, see fig. 1). Accuracy of the $L$, estimated without standards, is essentially worse (> 10%) than that of the interatomic distances (see above) because of the errors in $K$, $B$ and the instrumental distortions.

We do not use the transmission electron microscopy (TEM) to investigate the nanocrystals in the silicate glass for the following reasons: i) very thin films of the material are required to investigate by TEM, and preparation process of them can significantly affect the structure of nanocrystals in a glass; ii) these thin films of the silicate glass loose the shape due to firing up to 700 – 800 K and form drops, so TEM investigations become impossible.

3. Results and Discussion

The X-ray diffraction patterns for glass1 before and after doping are shown in fig. 1. From Scherrer’s formula for CuK$_\alpha$ radiation ($\lambda = 0.15418$ nm) we evaluate the size of nanocrystals $L \approx 0.87$ nm in the undoped glass1 and $L \approx 1.53$ nm in the doped glass1. The same values were found for the glass2 as well. The main reflexes of polymorphs of silica and the lead silicates are in area $d = 3 - 5$ Å. This conforms to wide halo at $2\theta \approx 31.86^\circ$ for nondoped glass1 (having molecular composition 2SiO$_2$-PbO) (fig.1).

![Figure 1. X-ray diffraction pattern for glass1 before and after doping. Sharp peaks are due to relics of RuO$_2$. B is the line broadening at half maximum of intensity (in radians) (1)](image)
sume the free charge carriers concentration \( n \) does not change. Sharp increase of the \( R(T) \) and \( S(T) \) at \( T > 800 – 900 \) K is the result of the structural transitions of silica and lead-silicate nanocrystals because the relict crystals of RuO\(_2\) do not have appropriate variations (fig. 4). This statement follows from the fact that increase of the interatomic distances in solids leads to decrease of its electrical conductivity. In the case of RuO\(_2\) crystals investigated, we have the opposite situation – lattice parameters, both \( a \) and \( c \), decrease in the temperature range 800 – 1000 K, where resistance \( R(T) \) of the sample increases (please compare fig. 2 and 3 with the fig. 4).

It is noteworthy that anomalous behavior of the thermal expansion of RuO\(_2\) crystals in \( a \) direction takes place (fig. 4) – extension is replaced by constriction in the temperature range 800 – 1000 K followed by extension again.

One can see from fig. 2 and 3 that the temperature dependences of \( R \) and \( S \) are very weak and the value of \( S \) is few or ten \( \mu \)V/K only at \( T < 800 \) K for doped glasses.

After maximum of \( R(T) \) the doped glass turns into typical semiconductor having band gap width between 0.05 and 1.5 eV for various glass compositions and doping levels (fig. 5). This means that the structural transition shifts away the impurity subband from the top of the glass valence band.

The comparison of the unit cell parameters of low-temperature \( \beta \)-quartz with the size of nanocrystals in the glass shows that the last one consists of 8 – 60 unit cells, or 24 – 180 atoms of Si, enclosed by mostly disordered layer. The effect of this layer on structural transitions of nanocrystals is not clear yet. In the case of the lead-silicates having larger unit cells, the number of the unit cells in the nanocrystals is smaller than that of the quartz.

![Figure 2](image2.png)

**Figure 2.** Temperature dependence of the resistance \( R(T) \) and the thermopower \( S(T) \) for the doped glass 1.

![Figure 3](image3.png)

**Figure 3.** Temperature dependence of the resistance \( R(T) \) and the thermopower \( S(T) \) for the doped glass 2.

![Figure 4](image4.png)

**Figure 4.** Temperature dependence of the lattice constants of RuO\(_2\) crystals in the free powder in \( a \) and \( c \) directions.

![Figure 5](image5.png)

**Figure 5.** Temperature dependence of the conductivity \( \gamma(T) \) after maximum for the samples of the doped glass1 (1) and glass2 (2 – 6) with RuO\(_2\) content about 16 wt % (1, 2), 20 wt% (3, 4) and 30 wt% (5, 6). Activation energy of conductivity \( E_\sigma \) is about (eV): 1.77 (1); 1.54 (2, lower \( T \)) and 0.93 (2, high \( T \)); 0.9 (3); 0.52 (4); 0.05 (5) and 0.047 (6). The solid lines are the fit of the experimental data with the expression \( \ln \gamma = a + E_\sigma / (2kT) \).

4. Conclusions

Nanocrystals of silica and silicates with the size of 0.8 – 1.6 nm undergo structural transitions at the temperatures 800 – 1000 K, detected as sharp maxima of the resistance and thermopower of the lead-silicate glass, doped by RuO\(_2\). Before these maxima the temperature dependence of the parameters and the value of the thermopower are typical for metals, while after maxima resistance assumes an activation character with activation energy of 0.05 – 1.5 eV depending on the glass composition. It is shown that the RuO\(_2\) relict crystals are not responsible for these anomalies because of the lattice constriction in the temperature region of these maxima (800 – 1000 K) and reduction of their resistivity. At maxima the value of the resistance may be 6 – 10 times
higher than that at room temperature, and value of the thermopower is 10 – 100 times higher than at room temperature.

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