Atomic structure and mechanical response of coincident stacking faults in boron suboxide

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ABSTRACT
We report the atomic structure of coincident stacking faults (SFs) in superhard boron suboxide (B₆O) by combining annular bright field scanning transmission electron microscopy and quantum mechanics (QM) simulations. Different from simple SFs, which only lead to the symmetry breaking, the coincident SF junctions in the complex B₆O result in local chemical configuration changes by forming an abnormal three-oxygen-atoms chain linking boron icosahedra, instead of the regular two-oxygen-atoms chain in a perfect B₆O crystal. QM studies demonstrate that coincident SFs lead to the decreased shear strength under pure shear and indentation conditions and are responsible to the initial failure and amorphization of B₆O.

IMPACT STATEMENT
Combining ABF-STEM and MD simulations, we demonstrated that the coincident SFs lead to the decrease of shear strength and are responsible for the initial failure and amorphization of B₆O.

Introduction
The combination of low density and super-high hardness is often desirable for structural materials and ballistic armor applications where both strength and weight are critical [1,2]. B₆O belongs to the icosahedral compounds with a rigid covalent bonding and has the promising properties of being ultra-strong (∼45 GPa in hardness) and lightweight (∼2.6 g/cm³ in density) [3–5]. Technically, boron suboxide (B₆O) can be fabricated under ambient pressure without the requirements of extremely high synthesis pressures at high temperatures, unlike other superhard materials such as diamond and cubic boron nitride [2–5]. B₆O mainly exist in the form of a stoichiometric compound [2,6], which is different from boron carbide that has a wide solid solution range. The distinct properties arise from the unique atomic structure of B₆O in which two-oxygen atoms bond to the neighboring boron icosahedra (B₁₂) and do not form direct oxygen-oxygen chemical bonding in a rhombohedral unit cell [7,8]. As a result, the complex atomic configuration in B₆O has anticipated the high density of planar defects during the crystal growth [9,10].

It has been suggested that planar defects, such as twins, enhance the strength of metals and alloys, identical to that of grain boundaries (GBs) [11,12]. In particular, the interfaces of nanotwins strongly influence the mechanical and thermal properties by blocking dislocation movements [13,14]. Despite the fact that dislocations

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in covalently bonded superhard materials are usually sessile at room temperature due to high lattice resistance, it has been found that nanotwins can enhance the hardness, toughness and thermal stability of diamond, BN, B₄C and B₆O [15–18]. Similar to twins and GBs, stacking faults also have a planar feature and can lead to strong interactions with dislocations for interface strengthening. For instance, Jain et al. examined an Mg alloy and showed the enhanced strength while maintaining good ductility by introducing a high density of stacking faults, which impeded dislocation slip and promoted dislocation accumulation [19]. Despite the fact that numerous stacking faults (SFs) and coincident SFs have been observed in B₆O and other superhard ceramics [9,10,15–18,20,21], their structure and influence on the mechanical properties of the superhard materials have not been explored partially due to the lack of sufficient spatial resolution to image light elements on atomic scale. In this work we investigate local atomic structure of single- and coincident SFs in B₆O crystals by means of state-of-the-art aberration-corrected annular bright field STEM (ABF-STEM) and QM simulations. The local structural and chemical variations were characterized by the experimental observations and modeled by QM simulations, which provide atomic insights into the structure and effect of SFs on mechanical properties of B₆O.

Results and discussion

Figure 1 presents an atomic resolution image of a B₆O crystal viewed in [11̄1] zone axis orientation. A representative high-resolution TEM image (Figure 1(a)) shows the high-density stacking faults (yellow lines) and twins (red lines) within a B₆O crystal. The ABF-STEM image (Supplemental Material Figure S1 and Figure 1(b)) obtained from the same B₆O crystal along the [11̄1] direction and the growth of SFs predominately develops along {10̄1} planes. Strain map of mean dilatation ($\delta_{xy}$) and rotation ($\omega_{xy}$) components of the ABF-STEM atomic structure obtained parallel to SF planes using peak pairs (PP) method. PP strain map and rotations was calculated using (101) and (01̄1) structural reflections. A lattice strain of $\delta_{xy}$ within a 1 nm SF region is about $\sim$ 3–4%. The color ranges from $\sim$ 5% (black) to $\sim$ 5% (white), (d) Lattice rotation of two SFs represented in color code by black and white, with respect to defect-free crystal (red color). The color varies from $-\pi$ to $+\pi$ using same color code. Dotted circle area in the vicinity of SFs from image (b) reveals distortion without rotation from maps (c, d).

Figure 1. TEM characterization of planar defects and strain map analysis of B₆O. (a) High-resolution TEM image displaying the high-density SFs and twins in a single crystal B₆O viewed along [1̄1̄1] direction, (b) ABF-STEM image of B₆O shows the coincident of two stacking faults (SF) within a crystal grain. The SFs interface was marked with false-coding of green and yellow colors. Inset FFT obtained from the single crystalline B₆O grain of (b) is oriented along the [1̄1̄1] direction and the growth of SFs predominately develops along [1̄0̄1] planes, (c,d) Strain map of mean dilatation ($\delta_{xy}$) and rotation ($\omega_{xy}$) components of the ABF-STEM atomic structure obtained parallel to SF planes using peak pairs (PP) method. PP strain map and rotations was calculated using (101) and (01̄1) structural reflections, (c) A lattice strain of $\delta_{xy}$ within a 1 nm SF region is about $\sim$ 3–4%. The color ranges from $\sim$ 5% (black) to $\sim$ 5% (white), (d) Lattice rotation of two SFs represented in color code by black and white, with respect to defect-free crystal (red color). The color varies from $-\pi$ to $+\pi$ using same color code. Dotted circle area in the vicinity of SFs from image (b) reveals distortion without rotation from maps (c, d).
projection clearly shows icosahedral (B\textsubscript{12}) clusters in the form of atomic rings and in between a linear array of pair of oxygen atomic columns [the experimental details are described in the Supplemental Material].\textsuperscript{1} In addition, the image displays coincidence of two stacking faults, their interfaces are marked with false-coding of green and yellow colors (Figure 1(b)). An inset FFT pattern in Figure 1(b) indicates that the stacking faults growth were predominately along (101) and (011) crystal planes. At proximity of the SFs intersection region, there are visible local structural distortions as represented by white circle (see Figure 1(b)). Figure 1(c,d) shows the two-dimensional maps of the mean dilatation elastic strain ($\delta$\textsubscript{xy}) and rotation ($\omega$\textsubscript{xy}) components derived from the ABF-STEM (Figure 1(a)) by using peak pairs (PP) analysis. The $\delta$\textsubscript{xy} value marginally increases to $\sim$2–4% in a $\sim$1 nm width of SFs region as compared to that of defect-free B\textsubscript{6}O crystal. The $\omega$\textsubscript{xy} map (Figure 1(d)) elucidates the anticlockwise ($+\pi$) and clockwise ($-\pi$) structural orientation of SFs region as compared to defect-free region. By close inspection of Figure 1(c,d), the vicinity region of the SFs intersection does not undergo any structural rotation, as shown by dotted circle (Figure 1(d)).

Figure 2(a) is a low-pass filtered ABF-STEM image of Figure S1 illustrates the icosahedral atomic rings of boron (B\textsubscript{12}) atoms and the positions of oxygen atoms (O–O) in a rhombohedral crystal of B\textsubscript{6}O, which is imaged along the [1\overline{1}1] direction. Although atomic columns of boron (B) in individual icosahedra are difficult to illustrate directly due to the short bond length distances along the imaging direction and curved surface of the icosahedron, two-oxygen atoms as the bright spots linking icosahedra are visible vividly. A fault of atomic plane stacking sequence is represented by B\textsubscript{6}O-1SF and the atomic planes with two coincident stacking faults are denoted by B\textsubscript{6}O-2SF as shown in the white box regions. The oxygen atoms at both SFs rotate to an opposite direction as compared to the defect-free B\textsubscript{6}O crystal marked by the red dots (Figure 2(a)). The bond length of O–O atoms at the SFs is nearly identical with respect to the B\textsubscript{6}O crystal of about 3 Å, which is consistent with predicted structure [8,9]. Figure 2(b) is the zoom-in

**Figure 2.** Atomic resolution of stacking faults viewed along [1\overline{1}1] direction in a B\textsubscript{6}O crystal, (a) Low pass filtered ABF-STEM image showing icosahedral (B\textsubscript{12}) units with bound linear oxygen atoms (O–O). A fault of atomic plane stacking sequence represented by B\textsubscript{6}O-1SF; and the coincident of two stacking faults atomic planes denoted by B\textsubscript{6}O-2SF are shown in white box regions, (b) A magnified ABF-STEM taken from marked B\textsubscript{6}O-2SF region shows three-oxygen atoms linked to icosahedral (white arrows) at the coincident site of two SFs, (c) Structure model constructed using QM simulations based on experimentally observed SFs atomic structure in (b). The green and red balls representing the B and O atoms, respectively. The solid line represents the supercell boundary and the dashed lines are the experimentally observed SF structure, (d) The simulated structure is well matched with ABF-STEM image of B\textsubscript{6}O-2SF.
ABF-STEM image of Figure 2(a) at the proximity of SFs, which shows the bonding of three-oxygen atoms (O–O–O) to icosahedral as marked by red arrowheads. To examine the experimentally observed SF structure (Figure 2(a,b)), we constructed the atomic structure in which two SFs are presented with periodic boundary conditions as shown in the dashed line regions in Figure 2(c). This structure consists of 16 B_{12} icosahedra and 16 O···O chains in the supercell structure. The PBE optimized supercell structure has the lattice parameters of $a = 23.597 \text{ Å}$, $b = 5.015 \text{ Å}$, $c = 19.998 \text{ Å}$, $\alpha = 90^\circ$, $\beta = 90^\circ$, $\gamma = 44.261^\circ$. On the basis of the QM model, we simulated the ABF-STEM image of the SFs (Figure 2(d)). The excellent consistency between the experimental and simulated ABF-STEM images justifies the reliability of the QM model. It is interesting to notice that the O–O bond in the SF region (along the ‘a’ axis) is separated by the icosahedral B–B bond, leading to an isolated O atom (O16 in Figure 2(c)) among three icosahedra, as shown in the oval in Figure 2(c). The bond distances of this O16 atom with three nearby B atoms are only 1.443, 1.434 and 1.435 Å, which are shorter than the normal B–O bond distance in perfect B_{6}O (1.496 Å). However, the bond distances of O15 with three nearest B atoms increase to 1.596, 1.597 and 1.581 Å. Apparently, the local strains at the SFs (Figure 1) are associated with the structural distortions.

The SF structure leads to the energy increase of 4.49 eV per SF structure. The absolute and relative free energies of the B_{6}O-2SF structure were calculated and compared with those of SF-1 and R-B_{6}O (Table 1).

To understand how the SF structure affects the mechanical properties of B_{6}O, we first applied pure shear deformation along (001)[100] slip system and compared with the perfect rhombohedral B_{6}O [the computational details are described in the Supplemental Material] (see Note 1). It is worth to notice that the SF structure in simulations is orthorhombic. The slip system is perpendicular to the SF structure and gives rise to a larger shear strain within the SF region. The plot of shear stress vs shear strain is displayed in Figure 3(a). The ideal shear strength of the SF structure is 34.8 GPa at 0.209 strain, which is 3.1 GPa smaller than that of perfect B_{6}O (37.9 GPa) shearing along (011)[111] the slip system [20]. The SF structure is also sheared along the interface and much larger shear strength (44.8 GPa) was found, indicating that shear parallel to the interface is not favorable. The details can be found in the Supplemental Material (Figure S2). Therefore, the present of SFs lower the shear strength and weaken the B_{6}O crystal. It is worth noticing that nanotwins can strengthen materials such as metals and c-BN [12,16]. Here in SF-2 structure, the bond distances of O15 with three nearest B atoms increase by at least 7% compared to the normal B–O bond distance. This leads to the weakening of icosahedra around SF-2 structure, lower the critical shear strength for failure. Figure 3(b–d) displays the deformation process of SF structure subjected to shearing along the (001)[100] slip system. The intact structure is displayed in Figure 3(b). As the system is sheared to 0.231 strain (corresponding to a maximum stress of 37.3 GPa) the B23–O15 bond in the SF structure is stretched from 1.596 to 1.840 Å, as shown in Figure 3(c). As the system is sheared continuously to 0.254 strain, the B23–O15 bond breaks with the B23···O15 distance increasing to 3.384 Å. Meanwhile, the icosahedron containing B23 atom is deconstructed, as shown in Figure 3(d). This leads to that the structure fails and the shear stress drops to 27.8 GPa. It is worth noticing that one icosahedron in the neighboring SF region is disintegrated because of the similar bond broken process of B14–O32, as shown in the oval in Figure 3(d). Thus, the SF structure failure initiates from the weak SF region by breaking the icosahedron-chain B–O bonds.

We also examined the failure mechanism of B_{6}O-1 SF, as shown in Figure S3. As the shear strain increases to 0.299 which corresponds to the maximum shear stress of 46.9 GPa, the inter-icosahedral B–B bond at SF layer (e.g. B72–B76) is stretched from 1.70 to 2.60 Å, but it is not breaking yet. As the shear strain continuously increases to 0.322, the inter-icosahedral B–B bond is stretched to 3.23 Å and breaks, leading to the decrease of shear stress from 46.9 to 45.90 GPa. As the shear strain further increases to 0.345, the O–B bonds (e.g. O16–B80) break and O16–B76 bond forms. Then the icosahedra rotate without breaking the icosahedra, leading to the shear stress significantly drops. The B_{6}O-1 SF increases the strength compare to the perfect B_{6}O because the slip system along the SF is different compared to perfect B_{6}O [21]. In perfect B_{6}O, the most plausible slip system is (101)[111], while the shear along SF plane is along [001] < 100 > rhombohedral slip system.

Indentation experiments are used to estimate the hardness of materials. To mimic the stress conditions under indentation experiments [29], we applied biaxial shear strains on the SF structure and compared to that of perfect B_{6}O. The shear stress versus shear strain curves of the SF structure and perfect crystals under biaxial shear are displayed in Figure 4(a). The critical shear stress of SF

| Structure       | Single crystal B_{6}O | B_{6}O-1SF | B_{6}O-2SF |
|-----------------|-----------------------|------------|------------|
| Energies (eV/ B_{6}O unit) | –50.13               | –49.98     | –49.90     |
| Relative energy (meV/ B_{6}O unit) | 0                    | 0.15       | 0.23       |

Table 1. Absolute energies of B_{6}O for single crystal B_{6}O, B_{6}O-1 SF and B_{6}O-2 SF.
Figure 3. (a) The shear stress–shear strain relationship of $\text{B}_6\text{O}-2$ SF structure under pure shear were compared to $\text{B}_6\text{O}-1$ SF and single crystal $\text{B}_6\text{O}$. Snapshots of $\text{B}_6\text{O}-2$ SF (b) Intact structure, (c) Structure at $0.231$ strain corresponding to the maximum shear stress of $34.8$ GPa, (d) Failure structure at $0.254$ strain. The deconstructed icosahedra are in the oval.

The critical shear stress is significantly decreased as SF structure presents under indentation conditions. The deformation process for SF structure under indentation conditions is displayed in Figure 4(b–f). As the shear strain increases from the intact structure (Figure 4(b)) to $0.144$, corresponding to the shear stress of $24.8$ GPa, the B23-O15 bond is stretched from $1.596$ to $1.639$ Å (Figure 4(c)). The bond length increase is less than that of pure shear deformation because of the biaxial shear stress conditions. Then, the B23-O15 bond is broken as it increases to $2.665$ Å at $0.166$ strain (Figure 4(d)). The corresponding shear stress (the maximum shear stress) is just $24.9$ GPa. In comparison with pure shear, the maximum shear stress for the bond breaking of B23-O15 slightly increases and the icosahedral clusters are not deconstructed. As the shear strain increases to $0.187$, the shear stress decreases to $24.7$ GPa. Correspondingly, the B108 atom is stretched out from the icosahedron near the SF structure (Figure 4(e)) and two icosahedra are deconstructed. As the shear strain continuously increases to $0.209$, the shear deformation deconstructs the icosahedra with missing boron atoms in the previous step (Figure 4(f)). In addition, two additional icosahedra in the other SF region are deconstructed, as shown in Figure 4(f). This leads to the failure of SF structure by amorphization, accompanying with a significant drop of shear stress to $15.0$ GPa.

The failure mechanism of $\text{B}_6\text{O}-1$ SF under biaxial shear deformation is shown in Figure S4. As the shear strain increases to $0.276$ corresponding to the maximum shear stress of $41.5$ GPa, the icosahedral B-B bond at both side of SF (e.g. B8-B16) is stretched from $1.79$ to $2.14$ Å, but it is not breaking yet. As the shear strain continuously increases to $0.299$, the B8-B16 bond is stretched to $2.14$ Å and breaks, leading to a slight decrease of shear stress to $35.0$ GPa. The critical shear stress is significantly decreased as SF structure presents under indentation conditions.
stress from 41.5 to 39.9 GPa. As the shear strain further increases to 0.322, these icosahedra at both sides of SF are disintegrated, leading to a decrease of the shear stress to 32.2 GPa. At 0.369 shear strain, B–O bonds in the SF break, leading to the shear stress drastically decrease to 21.5 GPa and failure.

Conclusions

In this study, we have characterized the atomic structure and mechanical response of single- and coincident SFs using ABF-STEM and QM simulations. The ABF-STEM images reveal the coincident SFs junctions linked with three-oxygen atoms (O–O–O), instead commonly observed O–O chains bonded to icosahedral B₁₂ clusters in single SFs and perfect B₂O structure. The coincident SFs possess obvious local distortions with 3–4% dilatation strains, which lead to the increase of free energy as compared to single SFs and perfect B₂O structure. QM simulations indicate that failure under shear initiates from the distorted SF region by breaking the icosahedral-chain B–O bonds at a relatively lower shear stress. The critical shear stress of coincident SFs under the pure shear stress and indentation conditions along (001)[100] slip systems are about 9% and 33% lower than the shear strength of perfect B₂O. The weakening results from the preferential deformation and structure damage by amorphization at the defect sites. These results underscore the importance of crystal defects in the failure and damage of complex materials with ultra-high strength.

Note

1. See Supplemental Material, which includes Refs. [22–28], for (i) experimental details, (ii) computational details, (iii) Figure S1. Atomic resolution ABF-STEM image of SFs B₂O. The unsmoothed (Raw) ABF STEM image and FFT patterns clearly demonstrate single SFs (b and c) and coincident SF (d) at intersection region in a single crystal B₂O (a and e). (iv) Figure S2. The shear deformation along the SF plane in the coincident SFs structure, (a) Shear model, (b) Shear stress vs shear strain relationship showing a higher strength than slip system in Figure 3. (v). Figure S3. The pure shear deformation along the SF plane in the 1-SF structure: (a) Intact structure; (b) structure at 0.299 shear strain corresponding to the maximum shear stress; (c) at 0.322 shear strain just passing the critical shear stress; (d) failure structure at 0.345 shear strain. (vi) Figure S4. The biaxial shear deformation along the SF plane in the 1-SF structure: (a) Intact structure; (b) structure at 0.276 shear strain corresponding to the maximum shear stress; (c) structure at 0.299 shear strain; (d) failure structure at 0.322 shear strain; (e) failure structure at 0.369 shear strain.

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Disclosure statement
No potential conflict of interest was reported by the authors.

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