Research Article

Predicting Crash Frequency for Urban Expressway considering Collision Types Using Real-Time Traffic Data

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Current studies on traffic crash prediction mainly focus on the crash frequency and crash severity of freeways or arterials. However, collision type for urban expressway crash is rarely considered. Meanwhile, with the rapid development of urban expressway systems in China in recent years, traffic safety problems have attracted more attention. In addition, the traffic characteristics are considered to be a potentially important predictor of traffic accidents; however, their impact on crashes has been controversial. Therefore, a crash frequency predicting model for urban expressway considering collision types is proposed in this study. The loop detector traffic data and historical crash data were aggregated based on the similarities of the traffic conditions 5 minutes before crash occurrence, among which crashes were divided by collision type (rear-end collision and side-impact collision). The impact of traffic characteristics along with weather variables as well as their interactions on crash frequency was modelled by using negative binomial regression model. The results indicated that the influence of traffic and weather factors on two collision types shared similar trend, but different level. For rear-end collisions, crash frequency increased with lower average speed and high traffic volume under low speed limit. And when the speed limit is high, higher average speed coupled with larger volume increases the probability of crash. Higher average speed and traffic volume increase the probability of side-impact collisions, without being affected by the speed limit. The findings of the present study could help to determine efficient safety countermeasures aimed at improving the safety performance of urban expressway.

1. Introduction

With the rapid development of Chinese cities, residents’ demand for travel and the increasing number of motor vehicles put forward higher requirements for the operation efficiency of cities. Urban expressway is a key part of the city roadway networks, which is of great significance to improve the travel efficiency. Compared with main arterial roads, urban expressway is characterized by large traffic volume and higher speed [1], resulting in frequent traffic crashes in recent years. In 2017, 6652 road crashes occurred causing 1673 deaths and 6862 injuries along the urban expressway [2]. Analysing the influence factors of urban expressway traffic crashes and establishing a crash prediction model play important roles for improving traffic safety.

A large number of studies on crash prediction models were mainly carried out from the aspects of crash frequency estimation and the crash severity prediction at the macro level (e.g., yearly, monthly) [3–6]. The Highway Safety Manual (HSM) prediction model represents the most widely used approach for road safety assessment, developing the safety prediction procedures for rural highways, urban and suburban arterials in the 2010 version of the HSM [7]. Taking factors such as traffic flow, road geometry, and so on into consideration, the HSM provides a prediction method for estimating the expected average frequency of single- and multiple-vehicle fatal-and-injury crashes.
Understanding of the quantitative relationships between introduced to improve road capacity and safety. Speed Limits (VSL) or fundamental speed limit settings are considered to be one of the most important factors leading to safety effect are not consistent. The inconsistencies among identified [18]. The relationship between operating speed and crash occurrence was speed and traffic safety; additionally, a U-shaped relationship between operating speed and traffic safety to determine strategies to reduce the crash risk. Previous studies have shown positive associations of average speed with crashes [19], while single-vehicle crashes and fatal-and-injury crashes involving multiple vehicles increase with the increase of the average speed [20]. However, others have shown a negative or an insignificant relationship between average speed and crash risk [21, 22]. In addition, some scholars have suggested that the safety effect of average speed would vary with road types [23]. As for the impact of speed limit on crash risk, some studies have found that speed limit is positively correlated with crash frequency and severity [24], and high speed limit road sections are often associated with high crash risk. However, Gou et al. mentioned that the crash frequency may be reduced due to better road facilities with high speed limit sections [25]. What is more, the safety effect of speed seemed to be related to other traffic variables such as traffic flow. For example, Kononov et al. have shown that higher crash risk is associated with high-speed driving in high-density traffic flow [26].

In summary, most studies on traffic crash prediction mainly focus on the crash frequency and crash severity on freeway or intersections, while the study considering the collision type of urban expressway crash is rare. Moreover, the relationship between traffic characteristics and crash probability needs to be further discussed. Weather conditions have been found to be associated with accident risk, especially rainy weather [27]. This study explores the impact of traffic characteristics and weather variable on crash frequency. Data from Wuhan urban traffic management systems were utilized here and crashes are divided by collision type (rear-end collision, side-impact collision, etc.). Collisions are the most common type of collision [28], and other collision types are excluded from the analysis because of the limited number. Data aggregated following a condition-based approach to reflect the conditions prior to crash occurrence are more accurate [18]. Finally, the relationships between relevant factors and traffic safety were conducted using negative binomial regression model.

The remaining of the paper is organized as follows. The data are collected and the negative binomial regression model is proposed for crash risk assessment. Sections 3 presented and discussed the results and the verification of the model. The paper ended with conclusions and limitations and looked forward for further study.

2. Data Collection and Preparation

To predict the crash frequency of urban expressway, historical crash, real-time traffic, and weather data have been utilized. Two urban expressways crossing over the river in Wuhan were chosen to be the data collection area, totalling 3,986 meters per direction. Inductive loop detectors and video monitoring were installed in the study area to provide real-time traffic flow data. Considering the design characteristics of urban expressways, the two-way lanes were considered to be independent of each other. Three datasets were used to build the database: (1) historical crash data

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from January 1, 2018 to October 31, 2018. It was obtained from the traffic accident archives recorded by Wuhan Municipal Public Security Bureau in detail, including information concerning crash occurrence time, location, weather, and collision types. During the study, there were 536 crashes in total, in which 321 were rear-end collisions and 135 were side-impact collisions. Considering the high frequency of rear-end and side-impact collision, this study only discussed the impact of the crash occurrence contributing factors on these two kinds of collisions and finally obtained a total of 466 collision samples. Moreover, weather conditions were also extracted from this dataset, which were divided into two categories in this study to indicate whether it was rainy or not. When a crash occurs, its weather data is usually recorded accurately by professional traffic police based on the weather information collected by the nearest weather station; (2) roadway posted speed limit. The speed limit on the road, as the upper limit of real-time speed, has critical impact on crash risk. The speed limits of the urban expressway sections studied are 50 km/h and 70 km/h, respectively, and remained consistent during the study period; (3) traffic data detected by Loop Detectors (LDs) located along the study area. Lane-based average speed and total volume at 5-minute interval were provided by LDs data, which could provide analysis with high-quality traffic flow data. For each crash, Mile Marker (MM) or Chinese characters associated with the crash records were used to describe its location, and the traffic data can be exactly matched with crash data according to the occurrence location and time recorded.

In the raw data of the LDs, there are abnormal values caused by equipment problems and other random errors, which can be identified by setting appropriate value interval of parameters, so as to screen out the unrealistic value [29]. The invalid values of parameters include (1) speed < 0 km/h or speed > 100 km/h; (2) speed > 0 km/h and volume = 0; and (3) volume > 0 and speed = 0 km/h. Previous studies have shown that data aggregation has a significant impact on the results of the crash modelling. Abdel-Aty et al. compared the crash risk prediction effect of data aggregated at intervals of three minutes and five minutes and found that the latter provided more information for analysis and had better research significance [30]. The random noise can be effectively reduced by aggregating the data into five-minute intervals. Considering that the weather conditions generally do not change in a short period of time, the hourly collected weather conditions were matched with crashes to provide the weather information for model building [15]. In addition, traffic characteristics (average speed, traffic volume, etc.) 5 minutes just prior to the crash time had great contribution to their occurrence [29]. Therefore, the traffic data five minutes prior to the reported crash time and the weather conditions at the reported crash time were identified and defined as the precrash condition to construct the crash prediction model and finally obtain a total of 466 precrash conditions. For example, the crash occurred at 9:30; then traffic data from 9:20 to 9:25 (a 5-minute window) collected by the LDs closest to the crash occurrence location and the weather information extracted from the traffic accident archives were extracted to form the precrash condition as shown in Figure 1.

3. Methods

3.1. Variable Setting. Based on the impact of data aggregation on crash modelling, a scenario-based data aggregation approach of significance has been proposed to identify the traffic conditions just prior to the crashes which might lead to crashes. For the scenario-based analysis, crashes were aggregated based on the similarity of the traffic conditions just before the crashes as employed by Yu et al. [18]. Precrash conditions, coupled with speed limit, were used as the control variable to define the potential crash scenarios, which were classified into equal frequency categories [15]. Firstly, the average speed was divided into 25 equal groups with a 4-percentile step; then each speed quantile was divided into 3 categories with a 33-percentile step for traffic volume. Further, the sequence was followed by splitting the speed limit into two equal quantiles for each quantile of traffic volume. Similarly, the weather (rain/no rain) conditions were divided into two equal-frequency groups for each volume category. Finally, a total of 300 scenarios (i.e., 25 × 3 × 2 × 2) were created, representing all the possible traffic conditions just prior to the crashes.

The 300 condition-based scenarios were matched with crashes that occurred under these traffic conditions and the crash frequency of each scenario was expressed by collision types (rear-end collisions and side-impact collisions). Therefore, an analysis dataset was formed by aggregating crashes into the same scenario. The traffic characteristics of each scenario were represented by the median values of average speed and traffic volume. Since it makes sense to study the relationship between traffic variables and crashes further, the potential interaction among traffic variables also needs to be taken into account. In this study, multiple interaction terms were utilized to study their impact on crash frequency in addition to the individual traffic variables. Table 1 presents the summary statistics of the scenario-based dataset.

4. Modelling

Statistical counting models have been widely utilized for crash frequency prediction. The Poisson regression model is a basic model to analyse the impact of potential factors on crash frequency and requires the mean and variance of crash frequency to be equal [31]. However, the dispersion and low probability of traffic accidents do not satisfy the assumption of Poisson’s distribution. This phenomenon of variance bigger than the mean value is usually called overdispersion. The negative binomial regression model is an extension of the Poisson regression model to handle this problem by introducing an error term that obeys Gamma distribution on the basis of Poisson’s regression model. This study explored the relationship between independent variables and rear-end collision and side-impact collision by establishing two negative binomial regression models. The expected crashes can be expressed as follows:
\[ y_{ik} = \exp(\beta_{ik} X_{ik} + \epsilon_{ik}), \quad (1) \]

where \( \lambda_{ik} \) refers to the expected crash frequency for \( k \) collision type of the scenario \( i \). \( X_{ik} \) is a set of explanatory variables for \( k \) collision type, such as traffic volume, speed limit, etc. \( \beta_{ik} \) is the corresponding regression parameters to be estimated for \( k \) collision type. \( \epsilon_{i} \) is the error term, which follows the Gamma distribution, with a mean value of 1 and a variance of \( \alpha^{2} \). So, the variance of the crash frequency distribution is

\[ \text{VAR}[y_{ik}] = \text{E}[y_{ik}] [1 + \alpha \text{E}[y_{ik}]] = \lambda_{ik} (1 + \alpha \lambda_{ik}), \quad (2) \]

where \( y_{ik} \) represents the observed crash frequency for \( k \) crash type of the scenario \( i \), \( \text{VAR}[y_{ik}] \) represents its variance, and \( \text{E}[y_{ik}] \) is the expected crash frequency. Then, the probability density function of the negative binomial regression model is formulated as follows:

\[ P(y_{ik}) = \frac{\Gamma(y_{ik} + (1/\alpha))}{\Gamma(y_{ik} + 1)\Gamma(1/\alpha)} \left( \frac{\alpha \lambda_{ik}}{1 + \alpha \lambda_{ik}} \right)^{y_{ik}} \left( \frac{1}{1 + \alpha \lambda_{ik}} \right)^{1/\alpha}. \quad (3) \]

Among them, \( \Gamma(\cdot) \) is a Gamma function. When \( \alpha = 0 \), the negative binomial regression model is the same with Poisson’s regression model; when \( \alpha > 1 \), the data deviation is large; when \( \alpha < 1 \), the data deviation is small. Since the large deviation of traffic crash data, the negative binomial model is widely used for traffic crash prediction.

### 5. Performance Evaluation of Prediction

Akaike Information Criterion (AIC) and Bayesian Information Criterion (BIC) were used to test the overall goodness-of-fit. Note that lower values of these measures signify better statistical fit. To further evaluate the models, two forecasting accuracy measures were adopted: Mean Absolute Deviation (MAD) and Mean Squared Error (MSE) [32].

MAD describes the magnitude of average bias in model prediction:

\[ \text{MAD} = \frac{1}{n} \sum_{i=1}^{n} |y_{ik} - \lambda_{ik}|, \quad (4) \]

where \( y_{ik} \) is the observed crash frequency for \( k \) crash type of the scenario \( i \) and \( \lambda_{ik} \) is the predicted one.

On the other hand, MSE refers to the mean value of the square misprediction of the estimated models. MSE is computed as follows:

\[ \text{MSE} = \frac{1}{n} \sum_{i=1}^{n} (y_{ik} - \lambda_{ik})^{2}. \quad (5) \]

MSE and MAD can be used to describe the accuracy of the model fitting. In general, the lower the value indicated, the better the prediction of observed data. However, the range of their values is not limited, and the validity of the model is usually tested by artificially defining a reasonable range. Therefore, \( R^{2} \) is further introduced to describe the accuracy of the model, and its value ranges from 0 to 1. The larger \( R^{2} \), the better the model fitting effect, and when \( R^{2} \) is greater than 0.4, the model is considered to have a good fit.

\[ R^{2} = \frac{\sum_{i=1}^{n} (\lambda_{ik} - \overline{y_{ik}})^{2}}{\sum_{i=1}^{n} (y_{ik} - \overline{y_{ik}})^{2}}, \quad (6) \]

where \( \overline{y_{ik}} \) is the observed average crash frequency for \( k \) crash type of the scenario \( i \).

### 6. Results and Discussion

Given the 0.05 significance level, the models were fitted by the Maximum Likelihood Estimation (MLE) method with the help of STATA 15.0 software. All the traffic variables along with their multiplicative interaction combinations and

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**Table 1: Summary statistics of the scenario-based dataset.**

| Variable                              | Description                                      | Mean   | SD    | Min    | Max    |
|---------------------------------------|--------------------------------------------------|--------|-------|--------|--------|
| Average speed (km/h)                  | Median speed for the crash occurrence scenario   | 37.68  | 8.04  | 20.98  | 80.77  |
| Volume (vehicles in 5 min interval per lane, vehicles) | Median volume per lane for the crash occurrence scenario | 126.97 | 44.19 | 12     | 209.875 |
| Speed limit (km/h)                    | 50 km/h or 70 km/h                               | 60     | 60    | 50     | 70     |
| Weather                               | =0 if rain; =1 otherwise                         | 0.5    | 0.5   | 0      | 1      |
| Average speed * volume (km/h * vehicles) | —                                               | 4644.11| 1565.61| 547.68 | 8143.15|
| Average speed * speed limit (km/h * km/h) | —                                               | 2178.36| 641.01 | 1049   | 5653.9 |
| Volume * speed limit (vehicles * km/h) | —                                               | 7148.54| 2283.65| 840    | 10756.67|
| Crash frequency                       | Rear-end collisions                              | 1.07   | 2.09  | 0      | 10     |
|                                      | Side-impact collisions                           | 0.45   | 1.41  | 0      | 6      |

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**Figure 1:** The precrash condition.
rain were taken as explanatory variables in both multivariate models. The best fitted variable combination for crash frequency prediction included all traffic and weather variables plus the interaction between average speed and speed limit. The performance of prediction was evaluated and Table 2 presents the values of these measures.

The result shows that the negative binomial model has good prediction performance for the rear-end collision and the side-impact collision. The significant variables in the two models include average speed, traffic volume, weather, speed limit, and the interaction between average speed and speed limit. In Table 2, a positive (negative) sign for a variable in the crash count component indicates that an increase in the variable is likely to result in more (less) vehicle crashes. Some variables have similar influences on the two types of crashes. For instance, the parameter for traffic volume reveals a positive association with crash proportion in both models, indicating that the frequency of rear-end collisions and side-impact collisions will increase with the increase of traffic volume [7, 15, 18]. The estimated result of weather variable implies that the presence of rain has a negative effect on crash rates, which is consistent with previous studies [33–35]. The high crash risk in rainy weather may have a certain relationship with poor road conditions and reduced visibility, which leads to longer stopping distance and longer reaction time. However, the parameter estimate value of the same significance variable is different in the two models, indicating that the same variable has different effects on the two types of crash frequency. For example, in the rear-end collision prediction model, the weather coefficient is −1.4399, while being −0.9787 in the side-impact collision prediction model, indicating that compared with the side-impact collision, rainfall has a greater impact on the rear-end collisions. The probability of rear-end collisions in a rainy environment is relatively high. It can be explained that when driving in rainy days, the stopping distance becomes longer due to the wetness of pavement, which are more likely to lead to rear-end collision.

Further analysis of the impact of road average speed and speed limit on the crash frequency was conducted. Due to the existence in interaction terms, although the estimation results of these two parameters were negative, we cannot draw the conclusion that they are negatively related to the crash frequency. In order to observe the contribution of the interaction between average speed and speed limit to the crash frequency, the crash rates are plotted in Figures 2(a) and 2(b) for the rear-end collision and the side-impact collision, respectively. The speed limit design of urban expressway generally ranges from 60 km/h to 100 km/h in China. In addition, considering that there was a research object with speed limit of 50 km/h in this study, the range of speed limit was determined to be 50 km/h–100 km/h, and the corresponding average speed range is 0 km/h–100 km/h. The results show that the influence of their interaction on rear-end collision and side-impact collision is different. For the rear-end collision, when the speed limit is low, the crash frequency will decrease with the increase of speed limit coupled with a low average speed. However, when the speed limit continues to increase, the crash frequency is positively related to the average speed. But for side-impact collision, no matter what the speed limit is, the average speed limit performs positive, indicating that the crash frequency increases with the rise of average speed.

The relationship between average speed, traffic volume, and crashes is further analysed, and the surface relationship diagrams of average speed and traffic volume with rear-end collision and side-impact collision under different speed limit conditions were plotted, respectively, as shown in Figure 3. For rear-end collision, the curves show that high crash risk associates with low average speed when the speed limit is low. When the speed limit is low, vehicles tend to drive at a lower speed, which to some extent promotes the occurrence of traffic congestion. Many studies, including those of Golob et al. and Christoforou et al., have shown that traffic congestion is one of the most significant precursors of rear-end collisions [11, 13, 36]. In the case of traffic congestion, drivers must adjust the speed in short time and short distance, making it more likely to lead to a rear-end collision, which is consistent with the results of this paper. When the speed limit is high, crash seems to be triggered at higher average speed and volumes. The vehicle tends to drive at a high speed under high speed limit. The vehicle inertia is too large to brake within a safe distance, leading to higher probability of a rear-end collision crash. In addition, it is clear that rear-end collision potential increase when the traffic volume is higher. This may be due to more interaction between vehicles at higher flow conditions leading to an increased tendency for rear-end collisions. Similar findings are also found in other studies [37].

The results in Figure 4 show that for the side-impact collisions, when traffic volume increase, the frequency of side-impact collision increases, which may be related to more frequent lane change behaviour of vehicles in high-flow conditions. This finding is similar to the work of Christoforou et al. who reported that side-impact collisions are more likely to be positively correlated with traffic volume [11]. Further, side-impact collisions are more probable to occur for high levels of traffic average speed [38]. One possible explanation could be that side-impact collisions are usually associated with lane change operations, which are more prone to crash at high speeds. The relationship
Figure 2: The impact of the interaction between average speed and speed limit on the crash frequency. (a) For the rear-end collision. (b) For the side-impact collision.

Figure 3: Relationships between speed, volume, and rear-end collision probability. (a) Speed limit $\leq 50\text{ km/h}$. (b) Speed limit $\leq 70\text{ km/h}$.

Figure 4: Relationships between speed, volume, and side-impact collision probability. (a) Speed limit $\leq 50\text{ km/h}$. (b) Speed limit $\leq 70\text{ km/h}$.
between these variables and the frequency of different crash types can be applied on safety improvement and management.

7. Conclusions

Traffic crash prediction is a hot topic in the field of traffic safety and keeps developing. In view of the shortage of urban expressway crash prediction and the controversial issue of the influence of speed on safety, the traffic and weather variables were used to predict the crash risk. This study developed crash risk analysis models for rear-end collision and side-impact collision with loop detector traffic data and historical crash data. For the purpose of exploring traffic conditions that leads to accidents, the data of Wuhan urban expressway were aggregated based on the similarity of traffic conditions in 5 minutes prior to crash occurrence. The impact of traffic variables along with their interactions and the weather condition on crash frequency was conducted by the negative binomial regression model. The results show that average speed, traffic volume, speed limit, and weather have significant impact on crash frequency and the influence of factors on two collision types is similar but with different degree. Specifically, the existence of rain increases the crash risk, especially for rear-end collisions. Higher traffic volume increases the crash risk. The impact of average speed on rear-end collision and side-impact collision on urban expressway is different. Specifically, under the lower speed limit, the probability of rear-end collision increases with the decrease of road average speed. At the higher speed limit, the probability of rear-end collision increases with the rise of road average speed. Regardless of the speed limit, with the increase of road average speed and traffic flow, the frequency of side-impact collision will increase.

In general, the specific combinations of traffic characteristics increase the probability of crash occurrences. These results are helpful to understand the crash risks under different traffic conditions and provide a basis for formulating traffic management countermeasures effectively. The results can be applied to real-time traffic management, where drivers can be warned via variable message sign once it is defined to be vulnerable to existing traffic conditions. In addition, the crash prediction model can also be applied to the evaluation and planning of road improvement projects when it is used to monitor the road safety level in real time. However, there are some limitations in this study. For example, due to the limited number of single-vehicle crashes, this study did not conduct the prediction model for it. Moreover, in order to better understand the impact of traffic characteristics on traffic crashes, further study of collision types is needed. At last, due to the existence of traffic heterogeneity, further crash risk analysis should consider the heterogeneous influence of various factors on traffic safety.

Data Availability

The crash data and traffic data are available upon request for research purpose.

Conflicts of Interest

The authors declare that there are no conflicts of interest regarding the publication of this paper.

Authors’ Contributions

Chaozhong Wu and Hui Zhang conceived and designed the study. Siyao Li, Hui Zhang, and Yafen Wang collected the data. Siyao Li, Hui Zhang, and Qi Zhang analyzed and interpreted the results. Siyao Li and Hui Zhang prepared the manuscript draft. All authors reviewed the results and approved the final version of the manuscript.

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