Diverse Structural Evolution at $z > 1$ in Cosmologically Simulated Galaxies

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ABSTRACT

From mock Hubble Space Telescope images, we quantify non-parametric statistics of galaxy morphology, thereby predicting the emergence of relationships among stellar mass, star formation, and observed rest-frame optical structure at $1 < z < 3$. We measure automated diagnostics of galaxy morphology in cosmological simulations of the formation of 22 central galaxies with $9.3 < \log_{10} M_*/M_\odot < 10.7$. These high-spatial-resolution zoom-in calculations enable accurate modeling of the rest-frame UV and optical morphology. This could depend strongly on dust radiative transfer, which we model using the Sunrise code. Even with small numbers of galaxies, we find that structural evolution is neither universal nor monotonic: galaxy interactions may trigger either bulge or disc formation, and optically bulge-dominated galaxies at this mass may not remain so forever. Simulated galaxies with $M_*/10^{10}M_\odot$ contain relatively more disc-dominated light profiles than those with lower mass, reflecting significant disc brightening in some haloes at $1 < z < 2$. By this epoch, simulated galaxies with specific star formation rates below $10^{-9.7}$ yr$^{-1}$ are more likely than normal star-formers to have a broader mix of structural types, especially at $M_* > 10^{10}M_\odot$. We analyze a cosmological major merger at $z \sim 1.5$ and find that the newly proposed MID morphology diagnostics trace later stages while Gini-$M_{20}$ trace earlier ones. MID is sensitive also to clumpy star-forming discs. The observability time of typical MID-enhanced events in our simulation sample is $< 100$ Myr. A larger sample of cosmological assembly histories may be required to calibrate such diagnostics in the face of their sensitivity to viewing angle, segmentation algorithm, and various phenomena such as clumpy star formation and minor mergers.

Key words: galaxies: structure — galaxies: formation — methods: numerical

1 INTRODUCTION

A galaxy’s morphology reflects structures that formed through complex and dynamic assembly processes. We obtain clues to these galaxy formation physics by measuring this morphology in large numbers of galaxies over cosmic time. Such surveys have demonstrated a tight connection between structural evolution and its implications for galaxy formation through other properties such as galaxy mass and star formation rate (e.g., Kauffmann et al. 2003; Wuyts et al. 2011; Omand, Balogh & Poggianti 2014). However, since we cannot directly watch galaxies evolve, the causal relationship between their formation physics and observed morphology is impossible to determine directly.

Hydrodynamical simulations of evolving galaxies allow us to calibrate these diagnostics by measuring their observability given a set of formation scenarios and physical processes (e.g., Jonsson et al. 2006; Rocha et al. 2007; Lotz et al. 2008b; Bush et al. 2010; Narayanan et al. 2010; Hayward et al. 2013; Snyder et al. 2013; Lanz et al. 2014). The quality and breadth of these experiments are limited by the availability of computational resources and the fidelity of models for galaxy physics such as star formation, supernovae, and the interstellar medium (ISM). It has only recently be-
come widespread to model the formation of galaxies \textit{ab initio} (e.g., Gueguen et al. 2004; Agertz, Teyssier & Moore 2011; Guedes et al. 2011; Marinacci, Pakmor & Springel 2013; Ceverino et al. 2014), and the realism continues to improve (Stinson et al. 2012; Hopkins et al. 2013; Torrey et al. 2014), albeit with still widely varying physics models (e.g., Scannapieco et al. 2012; Kim et al. 2014). Prior to these advances, they were limited to small numbers of isolated galaxies or mergers to inform common diagnostics of galaxy evolution, an approach with a significant limitation: they do not fully account for cosmological context, such as gas accretion and the breadth of assembly histories. In addition to mergers, models of high redshift galaxy formation (e.g., Dekel, Sari & Ceverino 2009; Dekel et al. 2013) have recently appreciated the tight coupling between gas accretion and disc evolution (e.g., Danovich et al. 2012; Cacciato, Dekel & Genel 2012; Dekel & Burkert 2013), as well as bulge and SMBH growth mediated by turbulent motions or violent disc instability (e.g., Bournaud et al. 2011; Porter et al. 2014) and the evolution of giant clumps (Dekel & Krumholz 2013). These important processes likely complicate interpretation of a given observation, and recent studies of galaxy morphology have begun to exploit simulations including them (e.g., Scannapieco et al. 2010; Pedrosa, Tissera & De Rossi 2014).

With the advent of deep, near-IR surveys and improving models, it is now possible to test the physics responsible for the emergence and evolution of galaxy structures in the early universe. In this paper, we analyze re-frame optical morphologies of galaxies forming in very high spatial resolution cosmological simulations, as if they were observed by the Hubble Space Telescope (HST), quantifying their dependence on time, mass, and star formation rate. Section 2 summarizes the hydrodynamical and dust radiative transfer simulations, their conversion into realistic mock HST images, and the pipeline for measuring photometry and non-parametric morphology, using analysis routines identical to those applied to distant galaxy surveys with HST such as CANDELS. Section 3 presents the predicted morphological evolution at $1 < z < 4$, using non-parametric quantitative measures, for simulated galaxies with $M_* \sim 10^{10} M_\odot$. We discuss implications of this evolution in Section 5 and conclude in Section 6.

2 SIMULATIONS AND MOCK IMAGES

Moody et al. (2014) presented basic details of the mock data pipeline, and a series of papers presented the full details of the zoom-in simulations (Ceverino & Klypin 2009; Ceverino, Dekel & Bournaud 2010; Ceverino et al. 2012; Dekel et al. 2013; Ceverino et al. 2014). We summarize here the elements essential to our morphological analysis.

2.1 Hydrodynamical Simulations

We analyze 32 cosmological hydrodynamical simulations calculated with the Eulerian gasdynamics + N-body Adaptive Refinement Tree code (ART, Kravtsov, Klypin & Khokhlov 1997; Kravtsov 2003) in a WMAP5 cosmology (Komatsu et al. 2009). In addition to gravity and gasdynamics, we apply sub-grid models for various physical processes, following Ceverino & Klypin (2009). They include treatments for the physics of gas and metal cooling, UV-background photoionization, stochastic star formation, gas recycling and metal enrichment, and thermal feedback from supernovae (Ceverino, Dekel & Bournaud 2010; Ceverino et al. 2012), plus a new implementation of feedback from radiation pressure and radiative heating by young stars (Ceverino et al. 2014 hereafter C14). These have been used to understand the gasynamical processes affecting the evolution of galaxy sizes and hence the emergence of compact red and blue galaxies at high redshift (Zolotov et al. in prep.). The simulations we analyze here are organized into 10 pairs, where each pair consists of a simulation with and without this new source of feedback (RP and no-RP), plus 12 simulations for which only the no-RP simulations were analyzed. At the masses we consider, the RP feedback models are roughly 50% closer than the non-RP simulations to the observed stellar mass-halo mass relation, achieving agreement to within roughly a factor of two in halo mass (e.g., Behroozi, Wechsler & Conroy 2013). Collisionless star particles form out of the low-temperature gas in a Monte Carlo fashion, following a prescription that recovers the observed relationship between gas surface density and star formation rate (Kennicutt 1998).

For our purpose, the essential outputs of the simulation are the three-dimensional positions, masses, and ages of these stochastically spawned star particles, and the three-dimensional metal mass density. The finest adaptive mesh refinement scale of the latter is 17–35 pc, leading to star particles representing $M \sim 10^3 M_\odot$.

We initialized the zoom-in hydrodynamical simulations by randomly selecting haloes with virial masses $10^{11} M_\odot < M_{200} < 10^{12} M_\odot$ and no ongoing major merger at $z = 1$ from a coarsely resolved N-body simulation $\sim 30$ Mpc across. We then re-sampled and re-simulated those regions in full hydrodynamics at high resolution with the physics models described above, in all cases to $z \sim 1$ and in some cases to $z \sim 0.7$. The galaxies forming in these simulations have $9.3 < \log_{10} M_*/M_\odot < 10.7$.

We stored the state of these simulations at a large number of cosmic times, with $\Delta z = 0.01$ at $0.5 < z < 4$, and subsequently analyzed a fraction of these, typically 20–100 per simulation, with the RP simulations sampled more finely than the no-RP simulations. In many cases we find similar results for the RP and no-RP simulations at the same cosmic time, so for clarity we typically plot the RP simulations only and highlight the key differences where appropriate. Figure 1 presents the basic global parameters – redshift, star formation rate, stellar mass, and halo mass – of the RP simulations studied here. The no-RP simulations have $\sim 50\%$ higher stellar mass at the same halo mass.

2.2 Radiative Transfer Calculations

We post-processed the galaxy simulation data into raw mock images using the dust radiative transfer (RT) code SNIRIS (Jonsson 2006, Jonsson, Groves & Cox 2010; Jonsson & Primack 2010), initialized with a pipeline based on the simulation analysis tool of Turk et al. (2011). We first assign to each star particle a spectral energy distribution (SED) based on its mass, age, and metallicity, set by the STARBURST99 stellar population models (Leitherer et al. 1999) with a Kroupa (2001) initial mass function. This SED is...
assigned as a source emitting uniformly from the nearest adaptive refinement tree cell. For full details, see Moody et al. (2014).

Then we calculate the 3-D dust density by assuming it is directly proportional to the metal density predicted by the ART simulations. We assume a dust-to-metals mass ratio of 0.4 (e.g., Dwek 1998; James et al. 2002), and the dust grain size distribution with $R=3.1$ from Weingartner & Draine (2001) updated by Draine & Li (2007). This model approximates the average dust observed in the Milky Way (e.g., Cardelli, Clayton & Mathis 1989; Gordon et al. 2003). For stars formed within the last $10^7$ yr, we assume an HII + photodissociation region (PDR) model by Groves et al. (2008) with a PDR covering fraction of 0.2. This uncertain factor leads to total SEDs matching many normal local galaxies (Jonsson, Groves & Cox 2010), but may underestimate the obscuration of massive gas-rich starbursts (e.g., Narayanan et al. 2010). With our focus on galaxies in $M \sim 10^{11.5} M_\odot$ haloes at $1 < z < 3$, with few major mergers, we expect the factor 0.2 is a reasonable choice. Even with the relatively small 17–35 pc scales resolved by these calculations,
the dust distribution on smaller scales—which we assume to be uniform—remains uncertain.

**SUNRISE** performs dust RT using an efficient parallel polychromatic Monte Carlo ray-tracing technique. Sources emit rays representing their SED, and as each ray propagates through the ISM and encounters dust mass, its energy is probabilistically absorbed or scattered until it exits the grid or enters the pre-defined viewing apertures (“cameras”). The output of the RT simulation is the SED at each of 600×600 pixels in each camera. We set 10 cameras, six of which we analyze in this paper. Of these six, two cameras are aligned to be edge-on and face-on to the angular momentum vector of each galaxy, respectively, and the remaining four are aligned randomly. For this work, we do not use the dust temperature and emission functionality of **SUNRISE**.

From these data cubes, **SUNRISE** creates raw mock images by integrating the SED in each pixel over the spectral response functions of a set of common astronomical filters, from the far-UV through IR. We perform this filter synthesis twice: first, we assume the source is at rest with respect to the observer, and second, we assume the source has a cosmological Doppler shift corresponding to the redshift at the cosmic time of the simulation (neglecting peculiar motions). We create analogous dust-free images in addition to the fully realized images. The spatial extent of each image increases with mass and cosmic time, and therefore so does the physical pixel scale of the raw mock images. We use pixel sizes of roughly 50–300 pc, sufficiently small to robustly simulate **HST** images of sources at $z \gtrsim 0.2$.

### 2.3 Image Realism

We include a number of **HST** UV through IR broadband filters in our **SUNRISE** pipeline. For this work, we select five filters to analyze, focusing on simulating a subset of the filters used by the CANDELS Multi-Cycle Treasury Project (Koekemoer et al. 2011; Grogin et al. 2011). They are:

- V (ACS/F606W)
- I (ACS/F775W)
- Z (ACS/F850LP)
- J (WFC3/F125W), and
- H (WFC3/F160W).

In the same manner as the CANDELS survey, this permits us to study, at high spatial resolution, a consistent rest-frame optical band across roughly $5 \times 10^9 \text{ yr}$ at $0.5 < z < 3$, mitigating the significant and confounding effect of the wavelength dependence of galaxy morphology. Additional filters are available in the **SUNRISE** pipeline for future analyses. In Figure 2 we show high-resolution noiseless simulated images of the ten RP simulations on which we focus, from $z = 2.3$ to $z = 1$. To create roughly rest-frame U-B-V images, at $z > 1.5$ we show the z, J, and H filters while at $z < 1.5$ we show i, z, and J.

From these, we scale the raw pixel sizes according to the angular size distance and fluxes for the luminosity distance at the redshift of each simulated source. Then we convolve these raw mock **HST** images with model point-spread functions (PSFs) appropriate for each instrument/filter combination (Krist, Hook & Stoehr 2011). Bin them to a pixel scale of 0.06 arcsec, and add noise approximating the total random background of the CANDELS-Wide survey in each filter (Grogin et al. 2011). The result is a database of model images at the resolution and depth of CANDELS-Wide. In Figure 3 we show the final mock **HST** images in the same filters and spatial scale as in Figure 2.

We can adjust at will the depth of the mock images, and in Section 3.7 we discuss a case where we required more depth to obtain reliable optical morphologies from the simulation (VELA28MRP; light green points).

### 2.4 Non-parametric Diagnostics

We locate and analyze sources in these images following closely the techniques used by CANDELS. We apply **SEXTRACTOR** (Bertin & Arnouts 1996) in dual-image mode to PSF-matched images, detecting sources in $H$, and use a multi-step algorithm to robustly locate small, faint sources while maintaining the contiguity of larger, brighter galaxies (Galametz et al. 2013). The result is a list of positions, sizes, and photometry for zero or more individually detected sources in each image. In this paper, we analyze the sources associated with the halo targeting described in Section 2.1 which we accomplish in practice by focusing on the bright source centered in each image.

For all such sources with $H < 24.5$, we measure non-parametric structural parameters in all five filters, including the Petrosian radius $r_P$, half-light radius $R_{1/2}$, Concentration (C) and Asymmetry (A) as defined by Conselice (2003), Gini and $M_{20}$ as defined by Lotz, Primack & Madau (2004), as well as three new indicators Multimode (M), Intensity (I) and Deviation (D) statistics by Freeman et al. (2013). These quantities describe the light profile of observed sources in a computationally efficient manner, and have been used to classify galaxy structural types and morphological disturbances in numerous surveys, including CANDELS (Peth et al. in prep.), Grogin et al. (2011) showed that the $H < 24.5$ magnitude selection cut is effective at identifying galaxies that are detected well enough to measure morphology in both non-parametric diagnostics (Lotz et al. 2011 e.g.) and visual classifications (Kartaltepe et al. 2014).

We use code originally developed for idealized merger simulations (Lotz et al. 2008b, 2010a, b) and also applied to galaxy surveys (Lotz, Primack & Madau 2004 Lotz et al. 2008a, 2011). We will first focus on the basic structural evolution of the cosmological simulations, but we return briefly to merger diagnostics in Section 4.1.

The Petrosian radius $r_P$ is defined such that the mean surface brightness in an elliptical annulus at $r_P$ equals 0.2 times the mean surface brightness within $r_P$. We define a galaxy’s pixels as those with flux values greater than the mean surface brightness at $r_P$.

We use the concentration parameter $C$ (Bershady, Jangren & Conselice 2000):

$$C = 5 \log_{10} \frac{r_{80}}{r_{20}},$$

where $r_{80}$ and $r_{20}$ are circular apertures containing 80% and 20% of the total flux within 1.5$r_P$ (Conselice et al. 2003).

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1. **SUNRISE** is freely available at http://code.google.com/p/sunrise
Structural Evolution in Mock Images

Figure 2. Noiseless high-resolution face-on images $\sim 40$ kpc across for the simulations with radiation pressure (RP), from $z \sim 2$ (bottom) to $z \sim 1$ (top) equally spaced in time. This shows approximately 20% of the simulation snapshots available, which are stored every $\sim 30$ Myr. Each column shows the evolution of a single galaxy; the border color corresponds to the points in Figure 1 and Table 1.

We derive the color and intensity at each pixel from synthetic mock images calculated with SunRISE, using the scaling algorithm by Lupton et al. (2004). To create roughly rest-frame U-B-V images, at $z > 1.5$ we show the z, J, and H filters while at $z < 1.5$ we show i, z, and J. Here we use the full pixel resolution from the simulated images, with no noise or PSF convolution. At low redshifts, some columns have missing data because the simulations were not run past that point. At high redshifts, some columns have missing data because a source was either not detected at all or not analyzed ($H > 24.5$) in our photometry and morphology pipeline from the CANDELS-like images (Figure 3).

of the galaxy centre defined by minimizing the Asymmetry parameter (Abraham et al. 1996).

Gini's coefficient ($G$) measures inequality among a galaxy's pixel flux values, varying from 0 (all pixels equal) to 1 (one pixel contains all flux). Abraham, van den Bergh & Nair (2003) first used it to characterize galaxy light profiles. $G$ increases with $C$ but does not depend on the location of the brightest pixels. Hence it detects not only compact spheroids but also galaxies with multiple cores. For a discrete sample, Glasser (1962) showed that $G$ can be computed as:

$$G = \frac{1}{|I_i|n(n - 1)} \sum_{i=1}^{n} (2i - n - 1) |I_i|, \quad (2)$$
Figure 3. Same as Figure [2] except showing realistic mock HST images. Each panel is 5.4 arcsec (∼ 40–45 kpc) across, and arranged from $z \sim 2$ (bottom) to $z \sim 1$ (top) equally spaced in time. Each column shows the evolution of a single galaxy; the border color corresponds to the points in Figure [1] and Table [1]. To generate these, we smoothed the images from Figure [2] with appropriate PSFs, binned them to a pixel scale of 0.06 arcsec equal to the CANDELS high-level science images [Koekemoer et al. 2011], and added a random background at the level appropriate for each filter [Grogin et al. 2011]. The result is a direct prediction for how these models would appear in CANDELS, allowing us to evaluate possible differences between observed stellar structures and galaxy formation theory. At low redshifts, some columns have missing data because the simulations were not run past that point. At high redshifts, some columns have missing data because a source was either not detected at all or not analyzed ($H > 24.5$) by our photometry and morphology pipeline based on these CANDELS-like images.

where we have $n$ pixels with rank-ordered absolute flux values $|I_i|$, and $|\bar{I}| = \sum_i |I_i| / n$, the mean absolute flux value. We follow Lotz, Primack & Madau (2004) in correcting $G$ using absolute values to mitigate the effect of noise-induced negative fluxes. This procedure recovers the true $G$ when $S/N \geq 3$ per galaxy pixel, which is true for almost all galaxies with $H < 24.5$ (see Section 3.7 for a counterexample).

$M_{20}$ is the spatial moment of a galaxy’s brightest quintile of pixel flux values, relative to its total moment (Lotz, Primack & Madau [2004]).

$$M_{20} \equiv \log_{10} \frac{\sum_i M_i}{M_{\text{tot}}}, \text{ for } \sum_i I_i < 0.2I_{\text{tot}}, \quad (3)$$
where

\[ M_{\text{tot}} = \sum_{i} M_i = \sum_{i} I_i \left( (x_i - x_c)^2 + (y_i - y_c)^2 \right), \]  

and \( x_c, y_c \) are the 2-D spatial coordinates of the galaxy centre, defined to minimize \( M_{\text{tot}} \).

The \( M, I, \) and \( D \) statistics were introduced by Freeman et al. (2013) to automatically identify disturbed morphologies in a way that reproduces the results of visual classifications. Let \( S_I \) be a superlevel set for \( I \), i.e., \( S_I \) is the collection of pixels within a galaxy’s segmentation map with intensity greater than or equal to a given threshold \( I \). Given this collection, one groups all contiguous pixels, orders the groups by decreasing area (such that \( A_{l,(i)} \) is the area of the \( i \)th largest group), and sets

\[ R_l = \frac{A_{l,(2)}}{A_{l,(1)}}, \]

The \( M \) statistic is then the maximum \( R_l \) value:

\[ M = \max_{l} R_l. \]  

\( M \), defined in this fashion, is not dimensionless, and thus a galaxy’s \( M \) value can depend on its angular size distance. While we choose to use \( M \) as defined above in this work, we will consider alternative definitions for future analyses, such as

\[ R_l = \frac{A_{l,(2)}}{A_{l,(1)}} \]  

where \( n \) is the number of pixels within the galaxy’s segmentation map, or

\[ R_l = \frac{A_{l,(2)}}{A_{l,(1)}}. \]

The normalization in Equation 7 fixes the possible range of \( M \) to the interval \([0, 0.5] \), where 0.5 would correspond to the situation, impossible to observe in practice, for which \( A_{l,(1)} = A_{l,(2)} = n/2 \). The normalization in Equation 8 fixes the possible range of \( M \) to the interval \([0, 1] \).

The \( I \) statistic is complimentary to \( M \) in that it takes into account pixel intensities. To compute \( I \), one traces maximum gradient paths from each pixel within a galaxy’s segmentation map to corresponding local intensity maxima, i.e., for a given starting pixel, one examines the eight surrounding pixels and moves to the pixel offering the largest increase in intensity, and repeats the process until a local maximum is reached. Each local maximum is thus associated with a set of pixels \( p \) with summed intensity \( I_p \). One sorts the summed intensities for each pixel set in decreasing order, yielding the values \( \{ I_{(1)}, I_{(2)}, \cdots \} \). The \( I \) statistic is then

\[ I = \frac{I_{(2)}}{I_{(1)}}. \]

Note that in practice, one obtains more accurate morphological classifications with \( I \) if the image data are slightly smoothed before \( I \) is computed. For instance, Freeman et al. (2013), who worked with HST images from the GOODS-S field, smoothed their image data with a symmetric Gaussian kernel with \( \sigma \approx 1 \) pixel.

The \( D \) statistic identifies galaxies whose shapes deviate from elliptical symmetry, and thus it serves a similar function to the \( A \) statistic defined above. One defines the intensity centroid of a galaxy as

\[ (x_{\text{cen}}, y_{\text{cen}}) = \left( \frac{1}{n} \sum_{i=1}^{n} x_i I_i, \frac{1}{n} \sum_{i=1}^{n} y_i I_i \right), \]

with the summation being over all pixels within the galaxy’s segmentation map. The \( D \) statistic is then

\[ D = \frac{\sqrt{\pi}}{n} \sqrt{\left( x_{\text{cen}} - x_{i,(1)} \right)^2 + \left( y_{\text{cen}} - y_{i,(1)} \right)^2}, \]

where \( x_{i,(1)}, y_{i,(1)} \) is the local maximum corresponding to the set of pixels with summed intensity \( I_{(1)} \), and \( \sqrt{\pi}/n \) is an approximate galaxy “radius” that acts to normalize \( D \).

In Section 3 we present the basic structural evolution of the simulated galaxies as if they were observed in CANDELS.
3 MORPHOLOGY EVOLUTION

In this paper, we explore the predicted global formation and evolution of basic galaxy types. Therefore we analyze primarily diagnostics of the overall light profile: $R_p$, $G$, $M_{20}$, and C. In this section we present the time-evolution of these parameters in the ten VELARP simulations, which have $9.2 < \log_{10} M_*/M_\odot < 10.3$. For this purpose, at a given redshift we focus on the HST filter corresponding most closely to the rest-frame B filter centered at $\sim 0.45\mu$m (Johnson & Morgan 1953):

- $z > 2.3$ H band $\sim 1.6\mu$m
- $1.5 \leq z < 2.3$ J band $\sim 1.25\mu$m
- $1.0 \leq z < 1.5$ Z band $\sim 0.85\mu$m
- $0.6 \leq z < 1.0$ I band $\sim 0.78\mu$m
- $z < 0.6$ V band $\sim 0.61\mu$m.

Each simulation consists of $\sim 200$ timesteps at which we conducted the radiative transfer post-processing. Of these, $\sim 50$ per simulation contained a source bright enough to be detected and its morphology measured from the mock images in at least one of the four randomly oriented cameras. We defined our nominal detection threshold in Section 2.4. Unless otherwise noted, we derive results only from this set.

3.1 Visual morphology

In Figure 3 we can directly observe some basic trends. Galaxies grow from bottom to top, where each column represents one of the ten RP simulations, organized from left to right by increasing stellar mass at $z = 2$ as in Table 1. At $z \sim 2$, most objects are compact, potentially hosting unresolved star-forming discs. By $z \sim 1.5$ these simulations host red compact bulges, and both disc and bulge components tend to grow between $z = 1.5$ and $z = 1$. At $z \lesssim 1.5$ we see extended star-forming discs around roughly half of the set. At $z \sim 2$, three simulations with $M_* < 10^{10} M_\odot$ are either undetected or do not satisfy our $H < 24.5$ selection criterion.

The incidence of large star-forming discs at $z < 1.5$ (top half) in the color images of Figure 3 appears to increase with stellar mass. We recover this trend qualitatively in the subsequent figures: galaxies in our sample with $M_* < 10^{10} M_\odot$ tend to be compact bulges at $z < 2$, while the higher mass model galaxy population tends to contain both disc-dominated and bulge-dominated objects. This trend may be expected as a consequence of increasing star formation efficiency as one approaches the peak of the stellar mass-to-halo mass relation from below. It may also reflect “disc settling” seen at $z < 1$ (Kassin et al. 2012) whereby more massive galaxies tend to have more ordered motions typical of rotating discs.

3.2 As a function of time

In Figure 4 we show how $R_p$, $G$, $M_{20}$, and C evolve with time in each of the ten RP models, at roughly the rest-frame B band as described above. For each bin evenly spaced in redshift, we plot the median value of the parameters measured within that bin. From these average quantities, the basic result is that the morphological evolution is not uniform. While these models are confined to a fairly small range in these quantities at $z \gg 2$, they evolve along diverse paths such that the distribution expands through $z \sim 1.5$. There are two simulations clustered at $G \sim 0.45$ ($C \sim 3$), corresponding to a relatively discy light profile, while the rest are more bulge-like, having median $G \gtrsim 0.53$ ($C \gtrsim 3.5$). This quantitative separation corresponds well with the visual impressions in Figure 3. All 10 RP simulations have similar median $M_{20}$ values during these times.

Size evolution of the simulated galaxies is similarly diverse. The bottom panel of Figure 4 shows that their radii ($r_p$) evolve roughly proportional to $(1 + z)^{1.5}$, with a wide scatter. Some galaxies (pink, orange, brown) have roughly constant median sizes at $1 < z < 3$, while others grow dramatically (light green; see subsequent figures and Section 4.3). Depending on their mass, the ten RP simulations have $r_p$ larger than $\sim 5 \times$ the PSF in the measured filter by $z \sim 2.5$. Thus the size and morphology measurements are at most times resolved well. We also estimated half-light radii, which are roughly $\sim 2 - 4$ kpc among the simulations we studied at $z = 1-2$. These are measured from roughly the rest-frame B filter and do not correct for PSF, and so may not accurately trace the 3D half-mass radii of these galaxies, which Zolotov et al. (in prep.) measured to be a factor of 2-4 smaller in several cases than those we measured here.

In Figure 5 we view the simulated galaxies’ evolution in $G$-$M_{20}$ space. We plot the same median values as colored points in three redshift bins. These points are evenly spaced in redshift, and therefore at a given epoch each simulation has equal weight. We plot dotted lines that coarsely separate observed galaxies into late types (bottom triangle), early types (right triangle), and mergers (upper left segment) following Lotz, Primack & Madau (2004). In addition, we compile all available models at each simulated timestep and plot them in contours of relative number density. This allows us to see how these values evolve in multiple dimensions: as in Figure 4 the median values split into a clearly wider distribution at $z < 1.3$, while the overall average trend with time is from the centre of the diagram upward and to the right, toward higher $G$ and lower $M_{20}$ (more bulge-like).

3.3 As a function of mass

In Figure 6 we separate these model data into four quadrants at $M_* = 10^{10} M_\odot$ and $z = 1.8$. Since a galaxy’s structure and star formation rate correlate with its mass in previous studies at these redshifts (e.g., Wuyts et al. 2011; Lee et al. 2013), we might expect to see a trend in our model structural diagnostics as a function of mass.

In the high redshift bin (left column), points and contours are centered in the diagram for both mass bins. This implies that the vast majority of model galaxies have disc-dominated profiles. Contours in the right column show that the overall trend toward the early-type region is present to roughly the same extent in both mass bins: some bulge growth occurs at all masses. Almost none of our models occupy the most extreme elliptical end of the $G$-$M_{20}$ locus (having $G \sim 0.6$, $M_{20} \sim -2.5$).

On the other hand, the models with $M_* > 10^{10} M_\odot$ contain more objects with robustly disc-dominated profiles ($G < 0.5$), and we see that these points (blue and gray) in the upper right panel are what gives rise to the structural diversity by $z \sim 1.3$ in Figures 4 and 5.
3.4 As a function of star formation

In Figure 7, we separate the models by specific star formation rate (SSFR = SFR/\(M_\odot\)) and redshift. We chose a limit of SSFR = \(10^{-2.7}\) yr\(^{-1}\) so that the “low star formation” bin contains a significant number of galaxies. However, this SSFR is a factor of \(\sim 10\) higher than common definitions of quiescent or non-star-forming levels (e.g., [Brammer et al. 2009]). Therefore this should be considered a cut that classifies galaxies into bins of normal star formation versus low star formation, as opposed to “star forming” and “not star forming”.

We find a difference in the average morphologies between the normal and low SF bins at \(z < 1.8\) (right column) in Figure 7. In the models, normal star-formers prefer the late-type (lower centre) region of the \(G-M_{20}\) diagram, while the low star-formers tend toward the observed position of early-type galaxies (Lotz, Primack & Madau 2004) in the right segment. One of the simulations that becomes disc dominated with time (blue; VELA27RP) is again visible as an outlier in the low star formation, \(z < 1.8\) panel. In general, normal star-forming galaxies are primarily disc-like, while low-star forming galaxies are either disc-like or bulge-like.

3.5 RP versus no-RP simulations

The phenomena described above are also present in the no-RP simulation set (Figures 6 and 8), which contains more than twice as many galaxies with synthetic images calculated, and in particular a broader range of masses. At \(z > 1.8\), the no-RP simulations have a somewhat greater fraction of low-mass galaxies that are very disc-dominated \((G \lesssim 0.45)\), in contrast to the RP simulations, but relatively fewer than at higher mass.

Overall, the general distribution of points in \(G-M_{20}\) and their dependence on mass and SFR, are very similar under the two different feedback models. Specifically, Figure 7 shows that in both the RP and no-RP simulations, nearly all of the vigorously star-forming simulated galaxies have \(G-M_{20}\) values in the bottom region of the diagram: they are disc-dominated light profiles. By contrast, the galaxies with SSFR < \(10^{-2.7}\) yr\(^{-1}\) are spread across the region separating disc-dominated and bulge-dominated.

In these cases of a minor shift or no change in the \(G-M_{20}\) distributions, it is difficult to infer anything concrete about the effects of RP feedback (c.f., [Trujillo-Gomez et al. 2013; Moody et al. 2014]). However, it is important not only to predict cases where observables will differ, but also to highlight certain trends which may be insensitive to differences in the model. In this case, \(G-M_{20}\) and (C) probe the kpc-scale distribution of observed optical light. In an individual galaxy, these measurements may differ quantitatively depending on whether the RP or no-RP feedback model is used (e.g., orange circles in upper right panel of Figure 6). We have not performed a systematic comparison on a per-galaxy basis. However, on average, \(G-M_{20}\) has the same distribution of values in both the RP and no-RP simulations. This does not rule out that other types of measurements may be significantly more sensitive to this difference.

3.6 Effects of dust

Dust affects the measured diagnostics in a predictable way. In particular, we find that the rest-frame B band \(G\) values increase by \(\sim 0.1\) when the SUNRISE dust RT is turned off, reflecting increased surface brightness of the few pixels containing young stars. Here, turning off dust RT corresponds with removing dust from the galaxies’ diffuse ISM component – there remains sub-grid dust obscuration by the PDR around stars with ages \(t < 10^7\) yr. Given our dust RT settings in Section 2.2, the former component has a significantly larger obscuring effect in the rest-frame optical.

Since the observed morphology distribution declines sharply at \(G > 0.6\) (especially for \(M_{20} \gg -2\); [Lotz et al. 2008a]), we conclude that an accurate treatment of dust at-
The kpc-scale morphological features probed by G in both the RP and no-RP simulations. This suggests that columns). Moreover, the overall distribution of points is similar in both the RP and no-RP simulations. Contours and points have the same meaning as in Figure 5, where colored circles correspond to the same haloes simulated in both the RP and no-RP simulations: colored triangles are the no-RP simulations that do not presently have counterparts with synthetic images. In both the RP and no-RP simulations, there are relatively more disc-dominated galaxies in the higher mass bin at $z < 1.8$ (right columns). Moreover, the overall distribution of points is similar in both the RP and no-RP simulations. This suggests that the kpc-scale morphological features probed by $G-M_{20}$ are somewhat insensitive to the detailed implementation of feedback from supernovae and massive stars. Instead, these features are likely governed primarily by the galaxy’s gas accretion and assembly history.

Without diffuse dust attenuation, the emergence of a detection is essential to bring these model diagnostics into agreement with data, similarly found by Lotz et al. (2008) in qualitatively different simulations. Removing dust also slightly increases the detectability of the models in our rest-frame optical, CANDELS-like mock images.

With diffuse dust attenuation, the emergence of a connection between morphology, mass, and star formation in these models remains qualitatively intact.

### 3.7 Incompleteness

For most of our mock images, the depth roughly associated with the CANDELS-wide fields was sufficient to obtain reliable morphology parameters at $z < 2$. At higher redshift, the falling signal to noise of the mock images causes either no source detection or sources fainter than those for which...
we believe a reliable morphological classification is possible ($H > 24.5$). However, some sources brighter than this magnitude cut are extremely red, causing issues owing to low signal-to-noise in our rest frame B band measurements (e.g., $z$, $I$, $V$ bands at $z < 1.5$). In particular, this effect caused errors for VELA28RP (black curves; Table 1), which has a very red, compact bulge and very faint, large disc at $z \lesssim 1.5$. This occurred for $\sim 2$ Gyr for this one of the ten RP simulations. At the CANDELS-wide depth, the simulated source did not have enough flux in the rest-frame B filter to reliably measure $M_{20}$ and $R_{\text{g}}$, in particular (other quantities were well measured). We re-analyzed its images with the background multiplied by a factor of 0.4 (“$\sim 1$ magnitude deeper”), which increased the signal-to-noise enough to reliably measure these quantities. In the black curves of Figure 4 and right-most column of Figures 2 and 3, this model now reflects an extremely concentrated central bulge and extremely low surface brightness disc, almost invisible when viewed face-on.

This brief experiment reflects the challenge in selecting and reliably classifying galaxies’ shapes in a fixed rest-frame filter. In particular, it highlights the known importance of using selection criteria independent of sources’ rest-frame filter, and of applying cuts that are complete to galaxies of the desired colors and radii in addition to stellar mass. This motivates a potential future project enabled by these simulations. For each simulated galaxy, we can search for the background level, pixel scale, and PSF size at which our automatically measured parameters converge (if any). The result would be a list of the telescope and survey parameters required to robustly classify each galaxy found in the simulations, regardless of its mass or type.

4 MERGER DIAGNOSTICS

Expanding on the general structural evolution of these cosmological simulations, in this section we apply merger diagnostics to the mock images. These qualitative studies are a precursor to a detailed study of the simulations’ merger histories in combination with morphology measurements.

4.1 Behavior of merger statistics in a cosmological major merger

While gas accretion is thought to be the primary driver of stellar mass assembly in most galaxies in the mass range we consider – $M_* \sim 10^{10} M_\odot$ at $z \sim 1$ – galaxy interactions and mergers may be important sources of gas and may trigger significant morphological changes in some haloes. Also, the rate of such events is observed to increase with redshift up to $z > 1$, and is predicted to be even higher at earlier times. The simulations we study here, and others, can serve as an important test-bed for predicting how such events will be observed, and for refining diagnostics to select and study them. Indeed, hydrodynamical simulations have enabled merger rate measurements at low redshift by predicting observability timescales of various indicators that are thought to be associated with merger events (Lotz et al. 2008b, 2010a, b; Snyder et al. 2011). However, such studies were limited to non-cosmological binary mergers, which most importantly do not account for the true cosmological complexity of gas accretion and merger events.

In Figure 9 we explore automated merger classifications. The $M$, $I$, and $D$ statistics were designed to automatically identify mergers in a way that reproduces the results of visual classifications (Freeman et al. 2013). The D statistic traces similar features as Asymmetry. In addition, we use $G-M_{20}$ to identify galaxies deviating perpendicularly from the bulge-disc locus, the evolution along which we have studied earlier in this paper. In detail, we define the $G-M_{20}$ merger statistic to be the point-line distance from the diagonal line that identifies mergers at low redshift: $G = -0.14 M_{20} + 0.33$ (Lotz, Primack & Madau 2004). Objects with negative values tend to be on the bulge-disc locus, and do not reflect obvious merger signatures. This merger statistic tends to highlight objects with multiple cores (large $M_{20}$) or merger-induced starbursts (high G). Variants of a $G-M_{20}$ statistic have been used, with other statistics, to track the galaxy merger rate versus redshift (e.g., Lotz et al. 2011).

Figure 9 shows the evolution of a single halo, viewed from five different directions, that experiences one or more mergers over 1 Gyr at $z \sim 1.6$. We define $z = 1.6$ as the merger time $t = 0$. We show mock HST $z-I-H$ composite images at the top, and encircle the SExtractor source segmentation map that fed into the morphology calculation. This segmentation is distinct from the final segmentations used to calculate either $G-M_{20}$ or $MID$, but demonstrates how any segmentation procedure depends on time and viewing angle during galaxy formation events. This uncertainty implies that care must be taken when interpreting variations, or lack thereof, in subsequent diagnostics.

This represents a fundamental difference between how surveys and simulations segment galaxies: group finders and merger tree codes can robustly isolate and track galaxies in three dimensions, but these identities are obfuscated when projected into multiple images. In principle, it is possible to locate a given galaxy in the final projected image after-the-fact, but there are simpler ways to enable this analysis. Specifically, we suggest an algorithm, which could be implemented as a feature in SUNRISE, to directly create “theoretical 2-D segmentation maps” in the same pixel sets as the mock images themselves, by projecting the theoretically segmented galaxy ID numbers. More specifically, the light from each star particle can be tagged with the galaxy or halo ID number in which it resides. For each pixel in the final projected image, we could find the galaxy ID number that contributes most to the total brightness at some chosen wavelength. Then a useful data product would be an image whose pixels are registered to the synthetic galaxy image, and whose pixel values are the galaxy ID number chosen in the specified manner. This would allow direct cross-matching between subhalo finding and image diagnostics, and enable joint analyses of the mock-observed sources and theoretical galaxy assembly histories.

Here, we directly perform the observational segmentation procedures as done for the CANDELS non-parametric catalogs, and do not consider the theoretical catalogs of haloes, mergers, and histories. This limits the meaning we can assign to measurements from the mock images, but does allow us to track galaxies in time as they would be measured in surveys, and to consider the robustness and applicability of various diagnostics in Figure 9. We defined the merger
time \( t = 0 \) as exactly \( z = 1.60 \). Overall, we find that the merger classifiers we consider, \( G - M_{20} \) and MID, are sensitive at different stages of the merger process: the \( G - M_{20} \) merger statistic is activated in the early stage at \( t < 0 \) while MID are activated for an extended period after coalescence at \( t > 0 \). This owes in part to the segmentation issues discussed above, but since these issues are present in survey analyses, the evolving sensitivities of the diagnostics here are meaningful.

The long-term global structure evolves from \( G \sim 0.45 \) at \( t = -530 \) Myr to \( G \sim 0.52 \) at \( t = 550 \) Myr. The galaxy also becomes more centrally concentrated according to \( M_{20} \) and \( C \) at \( t > 0 \). However, the \( G - M_{20} \) merger statistic is enhanced more strongly during the early stage \( (t \sim -200) \) than the late stage \( (t \sim 300) \).

Thus in this case the late-stage merger signatures are obfuscated in \( G - M_{20} \) space by global structural evolution: the galaxy evolves in \( M_{20} \) such that the \( G - M_{20} \) merger statistic is lowered, leading to a false negative or marginal detections of mergers in such systems. In other words, the threshold for diagnosing a merger with \( G - M_{20} \) may depend on the source’s initial or evolving overall structure. To identify these mergers robustly, a separate diagnostic or visual inspection must be applied.

The M, I, and D statistics do not have the same false negatives at late times, but they are less likely to be enhanced at early times. In our implementation, MID and \( G - M_{20} \) use different segmentation algorithms, a procedure to which both diagnostics are sensitive. For example, the red and gray points are activated at \( t = -70 \) owing to projections yielding images with multiple apparent nuclei.

In Table 2 we summarize the observed timescales for this one merger example (VELA08, one of 22 non-RP simulations). There are other interesting such events among these simulations, which we discuss in Sections 4.2 and 4.3, and that we plan to analyze in greater detail in a future paper.

In some cases, the numerical values of the MID statistics can depend on the distance to the source. This is not apparent here owing to the slowly changing ratio between physical and angular size at \( 1 < z < 3 \), but can manifest in studies of nearby galaxies, or comparisons between low and high redshift. As a workaround, one can redefine \( M \) using Equation 7 or 8.

### 4.2 MID enhancement timescales

Figure 10 presents the fraction of time that the ten RP simulations spend above selected thresholds in the MID statistics. We focus on the fewer RP simulations owing to their much higher mock image time sampling. Thus the merger example in Figure 9 is not shown, but in any case it is not a significant outlier in the sense of its duration with enhanced MID. However, we notice two simulations which are positive outliers in this sense: the blue and gray points are at or near the maximal MID enhancement fractions in each parameter and threshold. The gray points are simulation VELA15MRP, and blue are VELA27MRP. Recall that these same two simulations follow a “low Gini” track in Figure 4 and are two examples (of ten) that evolve away from the bulk trend toward more bulge-dominated and instead become more disc-dominated with time. They are therefore also outliers in Figures 3, 6, and 7. We discuss this connection in greater detail in Section 4.3.

Other features in Figure 10 include: 1) up to roughly half of the simulations experience MID enhancement for a negligible fraction of time (\( \sim 1% \)), 2) all simulated galaxies spend \( \sim 50\% \) of their time with \( D > 0.1 \), implying that this low level of disturbance is common, 3) square points (edge-on views) tend to be MID-enhanced for longer than the circles (face-on) and other shapes, at least for the blue and gray points, suggesting that sources viewed edge-on are more likely to be identified as MID-enhanced than those viewed face-on.

Figure 11 presents this MID enhancement information in the form of cumulative distribution function (CDF) of event durations. Here, we identify individual events during a simulated galaxy’s history in which the MID statistics reside above certain thresholds, the same as in Figure 10 as viewed from each of the six cameras. For each threshold level, each event has a duration \( t \) given by the sum of the simulation timesteps that constitute the event as viewed by a given camera. Thus these measurements correspond to how observed sources might be expected to appear if we could observe them as they evolved in time. When the quantity drops below the threshold level, then the event ends. Note that this accounting separates the merger in Figure 9 into at least two distinct events.

The CDFs thus answer the following question: “If I observe a quantity \( Q \) with \( Q > Q_t \), what is the probability that \( Q > Q_t \) for a duration \( t \) or longer in the current event?” The answer to this question can only be predicted with a suite of hydrodynamical simulations plus mock observations. We show curves for three example threshold levels \( Q_t \) in each quantity. In a gray dashed curve, we plot the CDF of the time spacing between simulation output times measured in the synthetic images.

Roughly 50% of the total time experiencing enhanced MID is composed of very short (\( \lesssim 100 \) Myr) events, with CDF curves very close to the simulation time spacing CDF. For this small set of ten simulations – chosen to have no major mergers during the \( \sim 1 \) Gyr before \( z = 1 \) – it appears that other events, such as minor mergers or large star-forming clumps, can enhance MID with very short durations for total duty cycles greater or comparable to longer, more obvious merger events such as the ones in Section 4.1 and 4.3. This preliminary estimate of the observability timescales for the MID statistics implies that significant care must be taken when interpreting any small number of observations or simulations.

### 4.3 Merger statistics and disc growth

Here we connect the two major sections of this paper. In Section 3 we inspected the average morphology evolution of cosmologically simulated galaxies. We found that many galaxies with \( 9.5 < \log_{10} M_*/M_\odot < 10.5 \) evolve from being disc-dominated according to \( G - M_{20} \) at \( z \gtrsim 2 \) to having a wider distribution – more bulge-dominated galaxies – at \( z \sim 1 \). At least two simulated galaxies near the middle of this range are obvious outliers from this trend by \( z \sim 1.5 \) – their rest-frame \( B\)-band light becomes more disc-dominated with time, with obvious star-forming discs. Several other simulations have discs that become brighter but are less disc-
Table 2. Total timescales, in $10^6$ yr, for VELA08 major merger event in Figure 9. These values are the sum of time spent above the threshold levels indicated in the column headers. Values in parenthesis measure the sum in only the timesteps at $-500 < t < 0$, where $t = 0$ is defined as $z = 1.60$.

| Camera | shape/segmap color | $M > 1$ | $I > 0.1$ | $D > 0.2$ | all MID | $G$-$M_{20}$ merger |
|--------|--------------------|---------|-----------|-----------|---------|------------------|
| 5      | diamond/pink       | 320 (0) | 150 (0)   | 320 (0)   | 150 (0) | 470 (150)        |
| 4      | inverted triangle/blue | 0 (0)  | 450 (0)   | 150 (0)   | 0 (0)   | 310 (310)        |
| 3      | triangle/orange    | 470 (150) | 300 (150) | 300 (150) | 630 (150) |
| 2 (edge-on) | square/green       | 170 (0) | 0 (0)     | 300 (0)   | 0 (0)   | 320 (0)          |
| 1 (face-on) | circle/red         | 0 (0)   | 170 (0)   | 470 (150) | 0 (0)   | 640 (310)        |

dominated (higher $G$), Zolotov et al. (in prep.) showed that gas discs can re-form around compact bulges that recently formed from the unstable collapse (‘compaction’) of a star-forming disc, and we are likely witnessing the aftereffects of such evolution and subsequent star formation through $G-M_{20}$.

In Section 4.2 we noticed that these same two simulations spend the highest fraction of their time with enhanced MID statistics, especially viewed from the edge-on direction. We explore these two examples in greater detail in Figures 12 (VELA15MRP; gray symbols elsewhere) and 13 (VELA27MRP; blue symbols elsewhere). These figures follow Figure 9 by showing at the top composite color images of the same simulation timesteps from five camera angles, where the bottom two are the face-on and edge-on orientations (red and orange segmentation maps, respectively). We zoom in to the sources such that the field of view of each panel is 3.6 arcsec across. At the bottom we show several morphology statistics: $I$, $D$, $G$-$M_{20}$ merger statistic (Section 4.1), and $G$. We do not show the $M$ statistic because it behaved similarly to $I$ and $D$ in Figure 9. These RP simulations have very fine time sampling, and so we show all points for the morphology measurements, but sub-sample the images we show at the top of the figure. We do this by dividing the full time range into bins spanned by the individual image panels. From each bin, we select the timestep with the maximal sum of the $I$ statistic over all six camera angles, display those images in the top section, and show a larger plot symbol for the selected timestep in the bottom section. This allows us to display all quantitative morphology measurements while enabling us to compactly visualize the timesteps with enhanced $I$.

First, since many of the simulations are MID-enhanced for longer when viewed-edge-on, large clumps in the discs may contribute to these enhancements, and their origin may be due to in-situ or ex-situ (Mandelker et al. 2014; Mandelker et al. in prep.). This could arise from the increased line-of-sight star formation intercepted by these cameras observing clumpy star-forming discs (Moody et al. 2014). Indeed, several of the $I$-enhanced images of Figures 12 and 13 appear to be selecting in-situ clumps. This is true at $t \sim 4.8$ Gyr and $t \sim 6.5$ Gyr in Figure 12 and $t \sim 4.5$ Gyr and $t \sim 5.5$ Gyr in Figure 13. Thus we conclude that MID may in some cases be selecting clumpy, growing discs from $HST$ images at $1 \lesssim z \lesssim 2$.

However, at other times, MID is clearly triggered by mergers, such as at $t \sim 5.95$ Gyr in Figure 12 and $t \sim 3$ Gyr in Figure 13. In the former, the VELA15MRP simulation shows a bright blue region for a very short period ($< 100$ Myr). By inspecting the time evolution of individual mock images at their full field of view ($\sim 10$ arcsec or $\sim 80$ kpc), we robustly identified this bright blue region as a small galaxy that is merging with the primary galaxy. This and nearby timesteps have enhanced $G$, $I$, and $D$ statistics (also $M$, $C$, and $A$, not shown), while the $G$-$M_{20}$ merger statistic increases but remains below 0 through this period. This lack of a $G$-$M_{20}$ merger signature reflects the generally low $G$ value of this disc-dominated source: as in Section 4.1, we see that the ideal $G$-$M_{20}$ merger classification threshold may depend on the underlying morphology of the system.

This minor merger occurs at an interesting time during the total evolution of VELA15MRP: at $t \lesssim 5$ Gyr, this galaxy has a compact, red core with a faint disc. The galaxy is still forming stars, and is never “quenched” in terms of a very low SSFR ($< 10^{-11}$ yr$^{-1}$). This early-forming core is stable, with roughly the same brightness at $4 < t < 7$ Gyr. The faint star-forming disc appears stable until $t = 6$ Gyr, just after the merger event, after which it experiences a disc-wide starburst event. This event then dominates the total color and brightness of the source by $t \sim 7$ Gyr ($z \sim 1$): the compact core remains at seemingly the same brightness and size, while the disc grows vigorously around it. Contrast this with the steadiness of the discs in other RP simulations at $z \sim 1$: Figures 13 and 14. While we cannot conclusively identify the merger as the causal trigger of significant disc star formation here, it is an intriguing suspect. It is possible that it disrupts or adds to the galaxy’s gas reservoir in such a way as to enable significant star formation in the disc, or that the smooth accretion of gas is enhanced during this event.

Figure 13 shows VELA27MRP, the other RP simulation with a disc-dominated light profile that becomes more disc-dominated with time. Here, the structure of the source is roughly stable at $t \gtrsim 4$ Gyr (though the disc may be growing in size here). However, prior to this, this halo experiences a major merger at $t \sim 3$ Gyr ($z \sim 2.2$), as seen not only by the first two disturbed image panels but also by inspection of the time evolution of wider-field images prior to these: we robustly identify a merger event here. Indeed, before $t \sim 2.8$ Gyr this source is undetected in our CANDELS-wide-like photometry, and before $t \sim 3$ it has a magnitude $H > 24.5$ that disqualifies it from our morphological pipeline. Its H magnitude increases by at least $\sim 2$ mags from $z = 2.4$ to $z = 2.1$ and fluctuates by $\sim 0.5$ mag shortly thereafter, reflecting evolution after a major starburst event (SFR $\sim 1000 M_{\odot}$ yr$^{-1}$). This is supported also by the blue points in Figure 10 that are well above the SF main sequence at $z \sim 2.2$.

After the merger, at $t \sim 3.5$ Gyr, this source obtains...
Figure 9. An example galaxy merger at $z \sim 1.6$ in mock $z$-J-H CANDELS images of simulation VELA08 (non-RP; SUNRISE images of the RP version have not yet been calculated at the time of this writing). This shows the same halo viewed from multiple angles over $\sim 1$ Gyr in mock HST images $\sim 3$ arcsec across. Colors here represent different viewing directions, not different simulations: we outline the SExtractor segmentation maps on the images and plot the matched colored points in the graphs below. This shows how some diagnostics are sensitive not only to the merger stage, but also to the segmentation of galaxy sources, especially at early times. We also show a rough bulge-disc classification based on $G-M_{20}$: the light profile shape at $t = 550$ Myr ($z \sim 1.4$) is largely unchanged from its initial state at $t = -670$ Myr ($z \sim 2$).

A red bulge with properties – like VELA15MRP above – roughly constant with time for several Gyr, surrounded by a faint star-forming disc. This is seen not only in the images but also the values of $G$: $G > 0.5$ at $t \sim 3.5$ shrinking to $G \sim 0.4$ at $t \sim 6$ Gyr as the disc begins to dominate at later times. In this case it is even harder to identify the merger as the cause of disc formation. However, it is more likely that it is the cause of bulge growth at early times, and it may or may not have played a role in allowing the disc to grow at later times. The simulation we identified as having a large undetected disc (VELA28MRP; black symbols elsewhere; Section 3.7) evolves in a manner very similar to this example (VELA27MRP), but for brevity we do not show its evolution.
Structural Evolution in Mock Images

Figure 10. Fraction of time spent by the simulations above each of three thresholds in MID for the ten RP simulations studied in this paper. The rightmost panel shows systems that are enhanced in all three of M, I, D above the 1st, 2nd, and 3rd levels of their respective panels. Colors correspond with Table 1 and to the other plots in this paper. The six point symbols reflect the six cameras we used to “observe” each galaxy. Circles are face-on, squares are edge-on; triangles, inverted triangles, and diamonds are random cameras 3, 4, and 5 as in Table 2, stars are another random camera. Plotted x-axis values for a given simulation have a random shift for clarity. The blue and gray points – the two simulations that experience significant evolution toward disc-dominated morphologies in Figure 4 – are near the top of the distribution here, suggesting that the formation of discs at $z \gtrsim 1$ is linked to higher MID statistics. This likely owes to enhanced merger activity, the sensitivity of MID (especially the $I$ statistic) to bright clumps, or both.

Figure 11. Cumulative distribution function (CDF) of observed event durations above various threshold levels in MID, for the ten RP simulations studied in this paper. The dashed gray curve represents the CDF of the simulation timesteps. As an example, the blue curve in the left panel shows the probability that a galaxy observed with $M > 1.0$ will sustain at least $M = 1.0$ for $t_{\text{Gyr}}$ during the current event. At least roughly 50% of the observed events in these sets are consistent with a duration shorter than the available simulation timestep spacing. These are a combination of complex assembly histories, potentially clumpy or disturbed morphologies that are extremely short-lived, and noise. This motivates the need for significant cosmological statistics in simulations like these in order to capture the rarer longer-lived and more robust events. If instead these turn out to be representative of typical MID-classified mergers, then this implies that significant numbers of galaxies observed with merger-like (MID-enhanced) morphologies are not drawn-out major events but may be short-lived disturbances.

5 IMPLICATIONS

5.1 Connection between morphology, mass, and star formation

In the stellar mass range $10^{9.3} \lesssim M_\ast/M_\odot \lesssim 10^{10.7}$, we find that galaxies in the haloes selected here experience a wide range of structural evolution. While the majority of the simulated galaxies in this range tend to become more bulge-dominated with time, with increasing $C$ and $G$, and decreasing $M_{20}$, over 20% of our simulations evolve in the opposite sense. Recall from Section 2.1 that these were selected to have no major mergers ongoing at $z = 1$ (up to roughly $\sim 1$ Gyr prior), so this finding applies to only a subset of galaxies. However, since it is the subset with possibly fewer merger events, then we expect that the diversity of morphology tracks experienced in these galaxies at $1 < z < 2$ should be considered a lower limit to the variation experienced by the true galaxy population.

We find that some (at least 2/5) simulated galaxies in the top half of this mass range ($M_\ast \gtrsim 10^{10}M_\odot$) become more disc-dominated over time at $1 < z < 2$ (Figures 3 and 4). While not unexpected, this implies many galaxies at higher redshift ($z \sim 3$) may not evolve monotonically toward progressively earlier types at lower redshift. This must be considered when analyzing the demographics of quenching over cosmic time: galaxies observed to be quenched and/or compact may not always remain so. Indeed, van der Wel et al. (2014) find that galaxies at Of course, at these or somewhat higher masses, other forms of feedback – such as from SMBHs – may become important (e.g., Croton et al. 2006) and may prevent the growth of a star-forming disc in these cases.
Broadly speaking, the correlations of mass and SFR with observed morphology (measured by $G-M_{20}$) are the same in both the no-RP and RP feedback cases (Figures 6 and 8, Section 3.5). This implies that the most important factors in determining the existence of these correlations are realistic assembly histories and some self-regulation of star formation (e.g., Agertz, Teyssier & Moore 2011; Hopkins et al. 2013; Stinson et al. 2012; Marinacci, Pakmor & Springel 2013). The details of the model implementation will not change significantly how morphology measured with $G-M_{20}$ at $\sim$ kpc-scale resolution will trace the galaxy’s mass and SFR. Specific model choices can do better (or worse) at matching the distributions of mass and SFR (e.g., Trujillo-Gomez et al. 2013), in which case we predict that the number densities of galaxies as a function of $G-M_{20}$ will also be better (or worse) match. Also other types of measurements, such as detailed shapes (van der Wel et al. 2014) and/or clump statistics (Moody et al. 2014), likely depend strongly on the specific feedback implementation (C14).

With powerful feedback resulting from massive stars and supernovae, these models retain significant gas reservoirs. At low masses, the strong radiative feedback of C14 inhibits star formation at late times (Trujillo-Gomez et al. 2013), leading to fewer low-mass models with $G \lesssim 0.45$ (very disc-dominated) in the RP simulations compared with the no-RP simulations (at least at $z > 1.8$; Figure 6). The continued disc growth among the more massive galaxies in both sets owes to the fact that supernova or strong radiative feedback cannot completely prevent star formation in such haloes. This gives rise to increasing star formation efficiency.
5.2 Mergers

The response of these galaxies and their haloes to mergers appears difficult to generalize. We identified several merger events and find that while they are associated with bulge growth, they are also associated with disc growth in the subsequent $\sim 1 - 3$ Gyr. Image diagnostics such as $G-M_{20}$ and MID respond in various ways depending on the orbit, mass ratio, and viewing angle of the mergers, and they appear very sensitive to the segmentation algorithm, which during complex merger events can scramble galaxy identities.

The newly proposed MID statistics (Freeman et al. 2013) are activated for an extended period ($\sim 2 - 5 \times 10^8$ yr) during an obvious merger. However, the majority of MID enhancement events in these simulated galaxies are $< 100$ Myr, approaching the measurement limit set by the stored simulation time spacing.

MID are also enhanced during the periods of rapid disc formation. In some cases, these enhancements reflect minor merger events (potentially contributing to the disc formation), but in others they identify in-situ clumps of star formation. Our goal for a subsequent paper is to cross-match the detailed histories of these haloes with the suite of image diagnostics. This will enable us to derive ideal diagnostics...
and/or combinations of diagnostics to identify high-redshift galaxy mergers.

Moreover, comparison between the detailed merger histories of these simulations and synthetic images will enable us to determine how best to incorporate treatments of merger observability into simpler models of galaxy formation. For example, by linking image diagnostics to merger trees, we can predict the distribution of observed merger outcomes in semi-analytic or analytic models, allowing us to probe a broader set of assembly histories than are available in hydrodynamical simulations.

5.3 Future mock image science

The conclusions above imply that a large volume of simulated cosmological histories may be required to span the range of these outcomes and thereby accurately calibrate these diagnostics for use with high-resolution imaging of objects at $z > 1$. It is not known if or by how much a realistic cosmological sampling of galaxy interactions may alter the observability timescales of merger induced morphological disturbances or starbursts (e.g., Lotz et al. 2008 [Snyder et al. 2011]). And we have not yet performed a full accounting of the origin of the galaxy structures we observe forming in the present simulations: i.e., how observed structures relate to the full accretion and interaction histories of these haloes. Moreover, it is not yet clear how many simulated galaxies we require for this endeavor, but it is likely that we need at least several examples each spanning the desired range of density and mass. Thus we are motivated to analyze not only more of the high-resolution simulations discussed here, but also much larger mock image datasets that traces the morphology of each of thousands of galaxies at a variety of masses (Torrey et al. in prep.), even if their morphologies and time evolution are more coarsely resolved. Indeed, recent studies find that the combination of supernova and AGN feedback may naturally set the morphology–mass–star formation correlations in galaxy populations at low redshift (Snyder et al. in prep.). As the methods and availability of computing resources increase, we will be able to exploit not only statistical samples of models, but also finely detailed modeling in time and space.

6 CONCLUSIONS

We studied the emergence of basic morphological types in galaxies simulated in a cosmological context. Applying dust radiative transfer and stellar population synthesis to high-resolution cosmological hydrodynamical simulations, we observed the simulated galaxies as if they were sources detected by the CANDELS survey with HST. We then characterized their rest-frame optical structures as a function of time, mass, and star formation rate. This represents one of the most direct applications of cosmological simulations toward the interpretation of state-of-the-art observations of galaxy structure across cosmic time, setting the stage for statistical comparisons between galaxy formation surveys and simulations using identical tools.

In the simulations studied here, having $9.3 < \log_{10} M_*/M_\odot < 10.7$ at $z \gtrsim 1$, we find:

(i) On average, these simulated galaxies show more bulge-like light profiles as time passes. Quantitatively, the average locus of at least half of the model galaxies evolves from $(G, M_20) \sim (0.47, -1.7)$ at $z \gtrsim 2$, overlapping with late type galaxies, to $\sim (0.55, -2.0)$ at $z \sim 1$, entering the space occupied by observed early-type galaxies (e.g., E, S0, Sa), while not yet reaching the region occupied by $z \sim 0$ massive ellipticals $\sim (0.6, -2.5)$.

(ii) Galaxies simulated with and without this implementation of radiation pressure (RP) feedback both appear to have similar correlations of stellar mass and SFR with $G-M_{20}$. Therefore, the relationship between current star formation and some measures of galaxy structure in HST images of distant galaxies can be somewhat insensitive to the details of the feedback model. However, this model’s feedback does not include IR trapping, and therefore stronger models may lead to a larger effect.

(iii) $2 - 4$ of the more massive galaxies ($M_* > 10^{10} M_\odot$) have rest-frame optical light profiles that become more disc-dominated with time, implying that galaxies with bulge-dominated light profiles may not remain so forever.

(iv) A wide distribution of $G-M_{20}$ morphologies is apparent at $M_* > 10^{10} M_\odot$ and $SSFR < 10^{-9.7}$ yr$^{-1}$: the morphology distribution appears roughly bimodal between earlier and later types as defined by $G-M_{20}$ in the rest-frame $B$ filter. Normal star-forming galaxies ($SSFR \sim 10^{-9}$ yr$^{-1}$) have predominately disc-dominated light profiles.

(v) Merger diagnostics of cosmologically simulated galaxies are very sensitive to the merger stage and to the segmentation algorithm, or how nearby objects are identified and separated.

(vi) The observability timescales of a generic event (either mergers or clumpy star formation) in the newly proposed M, I, and D statistics are on average very short (< 100 Myr), at least among this initial sample of assembly histories.

(vii) In a major merger simulated at $z \sim 1.6$ and measured with default segmentation algorithms, the newly proposed M, I, and D statistics are activated at times distinct and complementary to classical indicators based on Gini-$M_{20}$; MID traces $\sim 0.5$ Gyr at later stages, much longer than the average event duration of $\sim 100$ Myr, while $G-M_{20}$ traces $\sim 0.3$ Gyr at earlier stages.

(viii) The $\sim 2$ of 10 simulations with obvious disc formation at $1 < z < 2$ also spend roughly 10% of their time with enhanced MID, reflecting giant star-forming clumps and minor mergers that contribute to disc assembly.

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