Photoproduction of massive gauge bosons in $pp$, $pPb$ and $PbPb$ collisions

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In this letter we present, for the first time, the results for the photoproduction of massive gauge bosons in proton – proton, proton – Lead and Lead – Lead collisions at the Large Hadron Collider (LHC), High – Energy LHC (HE – LHC) and Future Circular Collider (FCC). Predictions for the rapidity distributions and total cross sections are presented. We predict a large number of events in the rapidity range probed by the LHC detectors, which implies that this process can be used to probe the photoproduction of massive gauge bosons as well to perform the search of Beyond Standard Model physics.

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The experimental results for photon – induced processes at Tevatron, RHIC and LHC have motivated a series of studies that propose to test our understanding of different aspects of the Standard Model as well to constrain possible scenarios of the Beyond Standard Model (BSM) physics using the analysis of different final states produced in $\gamma \gamma$ and $\gamma h$ interactions at hadronic collisions (For a review see, e.g. Ref. [1]). In this letter we will analyze the possibility of improve our understanding about the couplings between the gauge bosons considering the photoproduction of $Z$ and $W$ in $pp$, $pPb$ and $PbPb$ collisions for the energies of the next run of the LHC, as well of the High – Energy LHC [2] and Future Circular Collider [3]. In particular, we will estimate, for the first time, the total cross sections and expected number of events considering the rapidity range covered by the LHC detectors. Our goal is to verify if the experimental analysis of this process is feasible, which will allow to use it to test the Standard Model predictions, as well to search effects from new physics.

The photoproduction of massive gauge bosons ($G = Z^0$, $W^\pm$) in hadronic collisions is represented in Fig. 1, where we have considered that both incident hadrons can be the source of photons. The experimental signature for such events is the presence of one rapidity gap, associated to the photon exchange, and one intact hadron in the final state. The associated total cross section is given by

$$\sigma(h_1 + h_2 \rightarrow h \otimes G + X) = \int d\omega \, n_{h_1}(\omega) \, \sigma_{h_1 \rightarrow GX} (W_{\gamma h_2}) + \int d\omega \, n_{h_2}(\omega) \, \sigma_{h_1 \rightarrow GX} (W_{\gamma h_1})$$

(1)

where $\otimes$ represents the presence of one rapidity gap in the final state, $\omega$ is the photon energy in the center-of-mass frame (c.m.s.), $n_{h_i}(\omega)$ is the equivalent photon flux for the hadron $h_i$, $W_{\gamma h}$ is the c.m.s. photon-hadron energy given by $W_{\gamma h}^2 = 2 \omega \sqrt{N_N}$, with $\sqrt{N_N}$ being the c.m.s. energy of the hadron-hadron system. Considering the requirement that photoproduction is not accompanied by hadronic interactions (ultra-Peripheral collision) an analytic approximation for the equivalent photon flux of a nucleus can be calculated, which is given by

$$n_A(\omega) = \frac{2 Z^2 \alpha_{em}}{\pi \omega} \left[ \bar{\eta} K_0(\bar{\eta}) K_1(\bar{\eta}) - \frac{\bar{\eta}^2}{2} U(\bar{\eta}) \right]$$

(2)

where $K_0(\eta)$ and $K_1(\eta)$ are the modified Bessel functions, $\bar{\eta} = \omega (R_{h_1} + R_{h_2})/\gamma_L$ and $U(\bar{\eta}) = K_1^2(\bar{\eta}) - K_0^2(\bar{\eta})$. Moreover, $\gamma_L$ is the Lorentz boost of a single beam and we consider $R_p = 0.6 \text{ fm}$ and $R_A = 1.2 A^{1/3} \text{ fm}$ in our calculations for $pPb$ and $PbPb$ collisions. For the photon spectrum associated to the proton we will assume that it is given by

$$n_p(\omega) = \frac{\alpha_{em}}{2 \pi \omega} \left[ 1 + \left( 1 - \frac{2 \omega}{\sqrt{N_N}} \right)^2 \right] \left( \ln \Omega - \frac{11}{6} + \frac{3}{\Omega} - \frac{3}{2 \Omega^2} + \frac{1}{3 \Omega^3} \right),$$

(3)

with the notation $\Omega = 1 + \left[ (0.71 \text{ GeV}^2)/Q_{\text{min}}^2 \right]$ and $Q_{\text{min}}^2 = \omega^2/\left[ \gamma_L^2 (1 - 2 \omega/\sqrt{N_N}) \right] \approx (\omega/\gamma_L)^2$. This expression is derived considering the Weizsäcker-Williams method of virtual photons and using an elastic proton form factor (For more details see Refs. [4, 5]). The photoproduction cross section for the $\gamma h \rightarrow GX$ process is given by
\[
\sigma_{\gamma h \rightarrow GX(W_{\gamma h})} = \int_{x_{\text{min}}}^{1} dx \sum qf f(x, Q^2) \hat{\sigma}_G(\hat{s}),
\]

where \( f_{q/h} \) are the parton distribution functions in the hadron target (\( h = p \) or \( Pb \)), \( x_{\text{min}} = M_Z^2 / W_{\gamma h}^2 \), \( \hat{\sigma}_G \) is the cross section for the subprocess \( \gamma q \rightarrow Gf \) and \( \hat{s} = x \cdot W_{\gamma h}^2 \). For \( G = Z^0 \) we have that \( q_f = q_i \) (See Fig. 1) and the subprocess cross section, \( \sigma_Z(\hat{s}) \), is given at leading order by \[ \hat{\sigma}_Z(\hat{s}) = \frac{\alpha_G F_{\gamma e}^2 M_Z^2}{\sqrt{2} \hat{s}} \left[ \left( 1 - 2 \hat{z} + 2 \hat{z}^2 \right) \log \left( \frac{\hat{s} - M_Z^2}{\Lambda^2} \right) + \frac{1}{2} \left( 1 + 2 \hat{z} - 3 \hat{z}^2 \right) \right], \]

where \( \hat{z} = M_Z^2 / \hat{s} \), \( g_q^2 = \frac{1}{4}(1 - 4|e_q| x_W + 8 e_q^2 x_W^2) \), \( e_q \) is the quark charge and \( x_W = 0.23 \). On the other hand, for \( G = W \), we have \( q_f \neq q_i \) and \( \hat{\sigma}_W \) is given by \[ \hat{\sigma}_W = |V_{1f}|^2 \left\{ (|e_q| - 1)^2 (1 - 2 \hat{z} + 2 \hat{z}^2) \log \left( \frac{\hat{s} - M_W^2}{\Lambda^2} \right) - \left[ (1 - 2 \hat{z} + 2 \hat{z}^2) - 2 |e_q| (2 + 2 \hat{z}^2) - 1 \right] \log \hat{z} \right\} + \left[ \frac{1}{2} + \frac{3(1 + |e_q|^2)}{2} \right] \hat{z} + 2 |e_q| + \frac{|e_q|^2}{2} (1 - \hat{z}) \right\} \]

where \( \sigma_0 = \frac{\alpha_G F_{\gamma e}^2 M_W^2}{\sqrt{2} \hat{s}} \), \( \hat{z} = M_W^2 / \hat{s} \) and quantities \( V_{1f} \) are the elements of the Cabibbo-Kobayashi-Maskawa (CKM) matrix. The scale \( \Lambda^2 \) in the Eqs. 5 and 6 is a cutoff scale that regulates the singularity present at LO when the final state quark \( q_i \) becomes collinear with the initial state photon. Such singularity does not occur at LO for a non-vanishing transverse momentum \( p_T \) of the massive gauge boson, since in this case the \( p_T \) of the boson has to be balanced by the final state quark. As in previous studies [9–11], we will assume that the nuclear parton distributions can be expressed as \( f_{q/A}(x, Q^2) = A \cdot R_q(x, Q^2) \cdot f_{q/p}(x, Q^2) \), where the function \( R_q(x, Q^2) \) parameterizes the nuclear effects in the parton distributions and is described by the EPPS16 parametrization [12].

The rapidity distribution for the photoproduction of massive gauge bosons in \( pp, pPb \) and \( PbPb \) collisions can be calculated considering that the rapidity \( Y \) of the boson in the final state is directly related to the photon energy \( \omega \) by the relation \( Y \propto \ln (\omega / m_G) \). Explicitly, the rapidity distribution is written down as,

\[
\frac{d\sigma}{dY}[h_1 + h_2 \rightarrow h \otimes G + X] = \left[ \omega n_{h_1}(\omega) \sigma_{\gamma h_1 \rightarrow GX} \right]_{\omega_R} + \left[ \omega n_{h_2}(\omega) \sigma_{\gamma h_1 \rightarrow GX} \right]_{\omega_L}
\]

where \( \omega_L (\propto e^Y) \) and \( \omega_R (\propto e^{-Y}) \) denote photons from the \( h_1 \) and \( h_2 \) hadrons, respectively. As the cross section increases with the energy, we have that the first term on the right-hand side of the Eq. 7 peaks at positive rapidities while the second term peaks for negative rapidities. Consequently, given the photon flux, the study of the rapidity distribution can be used to constrain the photoproduction cross section for a given.
FIG. 2: Rapidity distributions for the $Z^0$ (left panels) and $W^+$ (right panels) photoproduction in $pp$ (upper panels), $pPb$ (central panels) and $PbPb$ (lower panels) collisions.

energy. Moreover, the rapidity distributions for $pp$ and $PbPb$ collisions will be symmetric about midrapidity ($Y = 0$). In contrast, for $pPb$ collisions, $d\sigma/dY$ will be asymmetric due to the dominance of the nuclear photon flux, which is proportional to $Z^2$.

In Fig. 2 we present our predictions for the rapidity distributions for the $Z^0$ (left panels) and $W^+$ (right panels) photoproduction in $pp$ (upper panels), $pPb$ (central panels) and $PbPb$ (lower panels) collisions. We consider the planned center – of – mass energies for the next run of the LHC, as well for the future High – Energy LHC [2] and Future Circular Collider [3]. We have that the predictions for the $W^+$ production are larger than for the $Z^0$ one, which is expected from the results for the photoproduction of massive gauge bosons presented in Refs. [9, 11]. Moreover, we have that for larger energies the rapidity distribution increases and becomes wider in rapidity. As expected from our previous discussion, the distribution is symmetric for $pp$ and $PbPb$ collisions and asymmetric for $pPb$ one, with the maximum occurring for positive rapidities. Finally, the predictions for midrapidities ($Y \approx 0$) increase with the energy and are a factor $\approx 10^3$ ($10^6$) larger in $PbPb$ ($PbPb$) collisions than in $pp$ collisions.
In the Tables I and II we present our predictions for the total cross sections and number of events considering the rapidity range covered by a typical central detector (|Y| ≤ 2.0), as the ATLAS and CMS detectors, as well as for a forward detector (2.0 ≤ Y ≤ 4.5) as the LHCb detector. For pp/ pPb collisions we predict cross sections of the order of pb/nb/µb, with the results for a forward detector being, in general, smaller by a factor ≥ 3 than for a central detector. In order to estimate the number the events we will consider that the expected integrated luminosities in pp/pPb collisions for the next run of LHC and HE – LHC are \( \mathcal{L} = 1 fb^{-1}/1 pb^{-1}/10 nb^{-1} \), while for the FCC are \( \mathcal{L} = 1 fb^{-1}/29 pb^{-1}/110 nb^{-1} \). Moreover, we will also take into account the leptonic decay mode, with the associated branching ratios for the processes \( W^+ \rightarrow \mu^+ \nu_\mu \) and \( Z^0 \rightarrow \mu^+ \mu^- \) being 10.63 % and 3.3658 %, respectively. The results presented in the Tables I and II indicate that the number of events is large, especially for \( W^+ \) production at midrapidities and FCC energies. In principle, such large number will allow to perform the search of tiny effects, as those associated to the presence of anomalous couplings between the gauge bosons, which are a signal of BSM physics (See e.g. Refs. [10, 11, 14]). Such aspect will be investigated in a future publication.

Two comments are in order. First, in our analysis the contribution for the massive gauge boson production associated to the hadronic component of the photon, denoted resolved contribution, was not included. Such contribution implies that a \( G + jet \) final state can be produced via e.g. the \( qq \rightarrow gG \) subprocess. Previous studies have demonstrated that the resolved contribution slightly increases the magnitude of the cross section and is negligible for the production of a massive gauge boson with a large transverse momentum [6]. Second, our estimates were obtained at leading order. The next to leading order (NLO) corrections are predicted to increase the LO direct cross section by ≈ 10% [10]. As both corrections increase the cross sections, the results presented in this letter can be considered a lower bound for the magnitude of the number of events expected at the LHC, HE – LHC and FCC. We plan to perform a more detailed analysis, taking into account of these corrections, in a forthcoming study.

| \( pp \) collisions | \( \sigma(Z^0) [pb] \) | # events \( (Z^0 \rightarrow \mu^+ \mu^-) \) | \( \sigma(W^+) [pb] \) | # events \( (W^+ \rightarrow \mu^+ \nu_\mu) \) |
|---------------------|-----------------|-----------------|-----------------|-----------------|
| \( \sqrt{s} = 14 \) TeV | 5.67 | 100.0 | 32.35 | 3438.0 |
| \( \sqrt{s} = 27 \) TeV | 9.36 | 315.0 | 56.30 | 5984.0 |
| \( \sqrt{s} = 100 \) TeV | 22.69 | 764.0 | 142.80 | 15719.0 |

| \( pPb \) collisions | \( \sigma(Z^0) [pb] \) | # events \( (Z^0 \rightarrow \mu^+ \mu^-) \) | \( \sigma(W^+) [pb] \) | # events \( (W^+ \rightarrow \mu^+ \nu_\mu) \) |
|----------------------|-----------------|-----------------|-----------------|-----------------|
| \( \sqrt{s} = 8.8 \) TeV | 2.29 \times 10^4 | 77.0 | 11.17 \times 10^4 | 1187.0 |
| \( \sqrt{s} = 18.8 \) TeV | 5.99 \times 10^4 | 201.0 | 34.16 \times 10^4 | 3631.0 |
| \( \sqrt{s} = 63 \) TeV | 21.44 \times 10^4 | 20940.0 | 135.88 \times 10^4 | 418877.0 |

| \( PbPb \) collisions | \( \sigma(Z^0) [pb] \) | # events \( (Z^0 \rightarrow \mu^+ \mu^-) \) | \( \sigma(W^+) [pb] \) | # events \( (W^+ \rightarrow \mu^+ \nu_\mu) \) |
|---------------------|-----------------|-----------------|-----------------|-----------------|
| \( \sqrt{s} = 5.5 \) TeV | 0.49 \times 10^5 | 165.0 | 1.40 \times 10^5 | 1488.0 |
| \( \sqrt{s} = 10.6 \) TeV | 1.24 \times 10^6 | 417.0 | 4.74 \times 10^5 | 5638.0 |
| \( \sqrt{s} = 39 \) TeV | 5.26 \times 10^6 | 19487.0 | 27.60 \times 10^5 | 322726.0 |

**TABLE I**: Cross sections and associated number of events in the leptonic decay mode for the photoproduction of massive gauge bosons in pp/pPb/PbPb collisions considering the typical rapidity range covered by a central detector (|Y| ≤ 2).

**TABLE II**: Cross sections and associated number of events in the leptonic decay mode for the photoproduction of massive gauge bosons in pp/pPb/PbPb collisions considering the typical rapidity range covered by a forward detector (2 ≤ Y ≤ 4.5).
As a summary, in this letter we have performed an exploratory study and estimated, for the first time, the $Z^0$ and $W^+$ photoproduction in hadronic collisions at the LHC, HE – LHC and FCC energies. Our study is strongly motivated by the high photon–hadron luminosity present in hadronic collisions at high energies, which become feasible the experimental analysis of different final state that can be used to test some of the more important properties of Standard Model (SM) as well to search by BSM physics. We have estimated the rapidity distributions for $pp$, $pPb$ and $PbPb$ collisions, cross sections for the rapidity ranges covered by central and forward detectors, as well the corresponding number of events in the leptonic decay mode. Our results indicate that the number of events is large enough to allow a future experimental analysis to probe the Standard Model predictions and possible scenarios of the BSM physics.

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