Orientation Dependent Interaction and Self-Assembly of Cubic Magnetic Colloids in a Nematic Liquid Crystal

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Spherical microparticles dispersed in nematic liquid crystals have been extensively investigated in the past years. Here, experimental studies are reported on the elastic deformation, colloidal interaction, and self-assembly of hematite microcubes with homeotropic surface anchoring in a nematic liquid crystal. It is demonstrated that the colloidal interaction and self-assembly of cubic colloids are orientation dependent. In a notable departure from the conventional microspheres, the microcubes stabilize diverse structures, such as bent chains, branches, kinks, and closed-loops. The microcubes reorient under external rotating magnetic field, thereby experiencing an elastic torque in the medium, which allows us to measure the magnetic moment through competition between elastic and magnetic torques. The findings envisage that the faceted magnetic colloids in liquid crystals are potential for developing new functional magnetic materials with specific morphologies.

1. Introduction

Self-assembly of colloidal particles into large ordered structures is a subject of immense interest in the field of soft matter, owing to the fundamental science and technological applications.\(^1\)–\(^4\) In aqueous suspensions, the colloidal interaction is mostly driven by entropic or electrostatic forces, which are short-range and isotropic, thus limiting the diversity in the resulting colloidal structures. Colloidal dispersions in nematic liquid crystals (NLCs) are very promising as they induce variety of topological defects and interact via long-range elastic forces.\(^5\)–\(^13\) They are especially interesting because of their ability to be assembled in a variety of ordered structures, such as bent chains, branches, kinks, and closed-loops. The microcubes reorient under external rotating magnetic field, thereby experiencing an elastic torque in the medium, which allows us to measure the magnetic moment through competition between elastic and magnetic torques. The findings envisage that the faceted magnetic colloids in liquid crystals are potential for developing new functional magnetic materials with specific morphologies.

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with their electric counterparts.\(^5\),\(^19\) The defect mediated elastic interaction gives rise to 2D and 3D colloidal structures and superstructures, bearing strong potential for photonic applications such as photonic bandgap crystals.\(^10\),\(^20\)–\(^22\)

Research on nematic colloids is mostly concentrated so far on spherical particles.\(^19\) Due to the advancement of synthesis and fabrication techniques, recently a surge has been observed in the number of investigations on nonspherical colloids, such as micro- and nanorods,\(^14\),\(^15\) ellipsoids,\(^23\) peanuts,\(^24\) microbullets,\(^25\) circular and polygonal platelets,\(^16\),\(^17\),\(^26\) handle-bodies of varying genus,\(^27\) and Mobius strips.\(^27\) These investigations have provided ample of new results on the topological defects and ensuing self-assembled structures. However, experimental studies on faceted colloids such as cubes with flat faces are largely unexplored. There are of course a few simulation studies on microcubes in NLC showing the sharp edges act as pinning sites of Saturn ring defect.\(^28\),\(^29\) The cube is modeled using a special case of the superellipsoid equation: \(x^{2m} + y^{2m} + z^{2m} = a^{2m}\), where \(m\) is a shape parameter, defining the roundedness of the corners. It represents a sphere of radius \(a\) for \(m = 1\), and a cube of side length \(L = 2a\) for \(m \rightarrow \infty\) as shown in Figure 1. As \(m\) interpolates the shape between a sphere and a cube, the defect loop evolves from a circular to distorted ring that wraps around the colloid while following only the edges.\(^28\)

In this paper, we for the first time report experimental studies on magnetic microcubes dispersed in a thin film of nematic liquid crystal. We study spontaneous orientation, elastic interaction and laser tweezer assisted colloidal assembly. We show that the cubic colloids stabilize diverse assemblies, which are not viable in spherical colloids. The cubic particles are made of hematite and hence respond to external magnetic fields, thereby enabling us to determine the magnetic moment from the competing effects of magnetic and elastic torques. The magnetic response provides an additional degree of freedom for manipulation and controlled assembly of colloids in liquid crystals.

2. Results and Discussion

The microcubes are nearly monodispersed with slightly round edges as seen in the scanning electron microscope (SEM) image presented in Figure 2a. The shape of our microcubes closely resembles the simulated cube with sharpness...
factor $m = 3$ as shown in Figure 1. The average length of the face diagonal is about 1.8 μm. Figure 2b shows a polarizing optical microscope (POM) micrograph with a few dispersed microcubes in 5CB liquid crystal. It is apparent that the microcubes have different orientations with respect to the rubbing direction, which cannot be determined conspicuously due to their small size. Nevertheless, careful observation at close-up reveals that there are mainly three types of orientations with distinct elastic distortions in which the first and second types can be identified as elastic quadrupoles (Figure 2c) and dipoles (Figure 2d); the third type (Figure 2e) exhibits an intermediate structure that does not resemble either of them. For a quadrupolar microcube, the face diagonal (Figure 2f), whereas the body diagonal of a dipolar microcube (Figure 2g) is parallel to the rubbing direction. In the intermediate structure, two opposite faces of the microcube are perpendicular to the rubbing direction (Figure 2h). Microscopic investigation on a large number of microcubes shows that majority (~80%) of the microcubes are quadrupolar type and about ~15% of them are dipolar type (Figure 2i). There are only ~5% microcubes exhibiting intermediate type director structure and the overall result is almost independent of the cell thickness.

Qualitative information about the anchoring of the LC molecules and the resulting defect is obtained by inserting a full waveplate ($\lambda$-plate) at an angle of 45° with respect to the crossed polarizers. The POM micrographs and the corresponding images taken with $\lambda$-plate are shown in Figure 3a,d,g. The $\lambda$-plate introduces a phase shift of exactly one wavelength (530 nm) between the ordinary and extraordinary wavefronts as a result of which mainly three colors are observed. The magenta color corresponds to either vertical or horizontal orientation of the director, whereas the bluish and yellowish colors correspond to clockwise and anticlockwise rotation of the director, respectively[15,19] as shown in Figure 3b,e,h. 3D schematic diagrams with induced defects of the microcubes are also presented in Figure 3c,f,i. Figure 3c shows that two opposite face diagonals of the microcubes are parallel to $n$ and the disclination ring (Saturn ring) encompasses the four vertices of a body diagonal plane. In Figure 3f, one of the body diagonals is parallel to $n$ and the microcube is accompanied by a point defect, closely resembling its spherical counterpart. The texture shown in Figure 3g evokes an interesting situation where the surrounding director profile as shown in Figure 3h is roughly in agreement with the dipole, except the point defect. This suggests that the intermediate texture corresponds to a defect structure, where the defect ring wraps the four edges of a face, which is perpendicular to the director $n$ as shown in Figure 3i.

In this case, the face normals of two opposite faces are parallel to $n$.

There are a very few computer simulation studies on the defects and pair interaction of cubic colloids using Landau–de Gennes (LdG) Q-tensor theory. Hung et al. showed that cubic nanocolloids mostly stabilize quadrupolar structure with a distorted disclination ring encircling the nanocubes, where the ring bends along six of the twelve edges of the cube[29]. Our experiments show that microcubes predominantly (~80%) stabilize quadrupolar structure, which is consistent with the predictions of the simulation (Figure 2i). Beller et al. predicted the polymorphism of the disclination ring, showing the rewiring of the defect ring to a new set of edges when the cube is rotated about a vertical axis through its center[28]. They showed that all these defect configurations of the microcubes correspond to the degenerate states of the LdG free energy. However, experimentally it is difficult to rotate the cube as described in the simulation. Hence, we looked at the Brownian motion of a quadrupolar microcube. The microcube executes rotational diffusion as a result of which the quadrupolar texture evolves continuously with time (Movies S1, Supporting Information). A few snapshots captured at different time intervals using polarizing optical microscope are shown in Figure 4. A movie taken with a $\lambda$-plate is also presented in Movie S2 (Supporting Information). It clearly shows the change of director with time at the vicinity of the microcube. Thus, the temporal change of the texture is due to the rotation of the cube which could lead to the rewiring of the disclination ring as predicted[28]. However, because of small size and the roundness of the edges, it is difficult to identify the different states with reconfigured disclination ring.

As a next step we study the elastic pair interaction of the microcubes using videomicroscopy technique. We trap two microcubes using laser tweezers and release them from a few micrometers apart and record their motion. The motion of the microcubes in the NLC is overdamped due to the high viscosity, hence the net force experienced by the moving microcubes at any instant is zero. This means the elastic force $F_{\text{elas}}$ is balanced by an opposing viscous drag force, $F_{\text{drag}} = -\zeta \dot{r}$, i.e., $F_{\text{elas}} + F_{\text{drag}} = 0$, where $\zeta$ is the drag coefficient, and $R(t)$ is the interparticle separation. The interaction potential $W(r)$ is obtained by integrating the drag force over the trajectory, i.e., $W(r) = \int F_{\text{drag}} \cdot dr$. Using methods similar to those reported in refs. [14,15], we measure the drag coefficients $\zeta_\parallel = 0.9 \times 10^{-6}$ kg s$^{-1}$ and $\zeta_\perp = 1.7 \times 10^{-6}$ kg s$^{-1}$, by measuring the anisotropic diffusion coefficients $D_\parallel$ and $D_\perp$ at room temperature ($T = 298$ K). The subscripts refer in relation to the director $n$. The drag coefficients weakly depend on the deformations hence, the average drag coefficient $\bar{\zeta} = (\zeta_\parallel + \zeta_\perp)/2 \approx 1.3 \times 10^{-6}$ kg s$^{-1}$ is used in calculating the interaction energy. The elastic force between two quadrupolar colloids is given by $F_E = -k/R^6$ and the corresponding intercolloid separation is given by[16,17]

$$R(t) = (R(0)^2 - 7\alpha t)^{1/7}$$

(1)

where $\alpha = K/\bar{\zeta}$ and $R(0)$ is the initial separation at $t = 0$ s. Figure 5a shows the variation of $R(t)$ of two quadrupolar microcubes and the nonlinear least squares fit to Equation (1). The
The binding energy of two quadrupolar microcubes is \( \approx 800 \ k_B T \) (inset to Figure 5a). The angle dependence of interaction of the microcubes, presented in Figure 5b, resembles to that of the spherical particles. For dipolar colloids, the interaction is given by \( F_e = -k/\alpha^4 \) and the time dependent interparticle separation can be written as\(^{16,17} \)

\[
R(t) = \left[ R(0)^2 - 5\alpha t \right]^{1/5} 
\]

(2)

Figure 2. a) Scanning electron microscope (SEM) micrograph of the silica coated hematite microcubes. b) Polarizing optical microscope (POM) micrograph of dispersed microcubes in 5CB nematic liquid crystal. POM micrographs of c) quadrupolar, d) dipolar, and e) intermediate type elastic distortions. f–h) Micrographs of the corresponding microcubes without polarizer and analyzer. i) Percentage of occurrence of three types of elastic distortions. About 200 particles are studied in two different cells with thickness 5 \( \mu \)m (red) and 8 \( \mu \)m (blue). Double headed arrows above \( \mathbf{n} \) denote the director, which is parallel to the rubbing direction.
Figure 3. a,d,g) Polarizing optical microscope (POM) and the corresponding λ-plate micrographs of three types of colloids. b,e,h) Constructed director profiles of each colloid. c,f,i) 3D orientation of the microcubes with induced defects. Defect rings (thick red lines) are pinned on the surface of the microcubes.

Figure 5c shows the variation of $R(t)$ and the corresponding least squares fit to Equation (2). The binding energy of two dipolar microcubes is $\approx 5000 \ k_B T$ (inset to Figure 5c), which is much larger than that of quadrupolar microcubes. The inter-particle separation $R(t)$ for two microcubes with intermediate structure (see Figure 3g) is shown in Figure 5e. $R(t)$ fits well to Equation (2) and the corresponding interaction energy is shown in the inset. The binding energy of two such microcubes is $\approx 1300 \ k_B T$ (inset to Figure 5e), which is much lower than the dipolar microcubes. Moreover, the angle dependence of the interaction of microcubes with intermediate structure is markedly different than the dipolar microcubes, where the point defects of both the colloids are on the same side (Figure 5d). In particular, the interaction between two intermediate microcubes is attractive at all angles (Figure 5f), whereas for the dipolar microcubes, it is either attractive or repulsive, depending on the approaching angles with respect to the director (Figure 5d). This unusual behavior of the microcubes with intermediate structure could be related to the relocation of the defect loop between the two orthogonal (with respect to $n$) faces while interacting. Taking advantage of the anisotropic interactions and the cubic shape, we prepared several equilibrium assemblies of the microcubes.

Figure 4. A few snapshots of rotational Brownian motion of a microcube at different time intervals (see Movies S1 and S2 in the Supporting Information).
Figure 5. Interparticle separation $R(t)$ with time of a pair of interacting a) quadrupolar, c) dipolar microcubes, and e) the microcubes exhibiting intermediate texture. Red lines are the least squares fits corresponding to equations $R(t) = (R(0)^2 - 7\alpha t)^{1/7}$ for quadrupolar and $R(t) = (R(0)^3 - 5\alpha t)^{1/5}$ for dipolar interactions. Corresponding potential energies ($W(r)$) in units of $k_B T$ are shown in the inset. b,d,f) Relative coordinates and resulting color-coded trajectories as a function of time for respective colloids. By “relative coordinate” we mean relative to the starting point of each trajectory.
with the help of the laser tweezers. Figure 6 shows a few non-linear chains, branches, kinks, 2D crystals, and closed-loop structures. The assembled structures of the microcubes are diverse when compared to that of spherical colloids which primarily stabilize either linear or zigzag chains. The segments which are parallel or perpendicular to the far field director are mostly composed of either dipolar or quadrupolar colloids, respectively. Microcubes with intermediate structure helps in forming branches, kinks, and loops. These structures are highly stable against thermal fluctuations and respond to external magnetic fields, hence could be useful as building blocks in making advanced magnetic materials with desired architecture. It may be mentioned that in addition to elastic interaction, the microcubes also experience magnetic dipole–dipole interaction and electrostatic repulsion due to electric double layer. Since the conductivity of the liquid crystal is very small, the electrostatic repulsion is expected to be negligibly small. The maximum magnetic dipole–dipole interaction (for parallel orientation) is estimated to be \( U_{\text{d}} = 100 k_B T \), which is smaller than the elastic interaction potential energy. Hence, the self-assembly of the microcubes is dominated by elastic interactions.

The microcubes possess a permanent magnetic moment along a direction which is nearly parallel to the body diagonal. In water, Earth’s magnetic field helps in forming linear chains, which are parallel to the field direction. However, in NLC, the orientation of the microcubes is mainly governed by the surface anchoring and the ensuing energy of the elastic distortion and is unaffected by the Earth’s magnetic field. To study the effect of applied magnetic field, we used two disc-shaped magnets and positioned them diametrically opposite on a circular track around the plane of the sample as shown in Figure S2 (Supporting Information). This arrangement provides an in-plane magnetic field which can be rotated around the cell by simultaneously rotating the two magnets. The strength of the field at the sample position measured by a magnetometer is 300 G. Although the individual microcubes respond to the rotating magnetic field, it is difficult to determine the angle of rotation conspicuously. Hence, we assembled dipolar and quadrupolar pairs of the microcubes using the laser tweezers and studied their magnetic response. Figure 7a shows a pair of quadrupolar microcubes, oriented perpendicular to \( n \) in the absence of applied magnetic field. When the magnetic field is rotated from \(-90^\circ\) to \(+90^\circ\) around the director, the body diagonal of the pair tends to follow the field direction as shown in Figure 7b. This means the direction of the resultant magnetic moment \( \hat{\mu}_{\text{eff}} = \hat{\mu}_1 + \hat{\mu}_2 \) is approximately parallel to the body diagonal of the pair as shown in Figure 7c. For a dipolar pair, the long body axis is parallel to the director in the absence of magnetic field as shown in Figure 8a. When the magnetic field is rotated, the short body axis of the pair tends to follow the field direction (Figure 8b). This suggests that the direction of the resultant moment \( \hat{\mu}_{\text{eff}} \) is along the short body axis of the pair as shown in Figure 8c.

The rotation of the microcube-pair increases the elastic energy, which opposes the effect of the magnetic torque \( \mu_{\text{eff}} \times \vec{B} \). In both cases, \( \mu_{\text{eff}} \) and the magnetic field \( \vec{B} \) make angle \( \theta \) and \( \phi \) with respect to the director \( n \). At equilibrium, the magnetic torque \( \mu_{\text{eff}} B \sin(\phi - \theta) \) is balanced by the gradient of the elastic energy \( -\partial U/\partial \theta \) and the torque balance equation can be written as

\[
-\partial U/\partial \theta + \mu_{\text{eff}} B \sin(\phi - \theta) = 0
\]  \( \text{(3)} \)

The enhancement in the elastic energy due to the rotation by an angle \( \theta \), in analogy with the electrostatic energy of a rod at a fixed potential is given by

\[
U = 2 \pi C K \theta^4
\]

where \( K \) is the effective Frank elastic constant and \( C = L/[2\log(L/d)] \), where \( L \) and \( d \) are the length and diameter of the assembled pair. The magnetic moments of both the pairs are determined from the slope of the equation \( B \sin(\phi - \theta) = (4\pi C K/\mu_{\text{eff}})\theta \). Figures 7d and 8d shows that \( B \sin(\phi - \theta) \) is linearly proportional to \( \theta \) with slopes 143 and 106 G rad\(^{-1}\) for quadrupolar and dipolar pairs, respectively. Taking \( C = 4.0 \times 10^{-6} \) m and \( K = 5 \times 10^{-12} \) N, the estimated magnetic moments for quadrupolar and dipolar

![Figure 6. Laser tweezers assisted assembly of microcubes with a,e,h) bent chains, b,i) branches, c,j) kinks, d) 2D crystal, and f,g) closed-loop structures. CCD images of the same are shown in Figure S1 (Supporting Information).](image-url)
pairs are given by $m_{\text{eff}} \approx 18 \times 10^{-15}$ and $24 \times 10^{-15}$ A m$^2$, respectively. Assuming that both the magnitudes are identical, the magnetic moment of a single microcube in quadrupolar pair is given by $\mu_1 = \mu_2 = \mu_{\text{eff}}/2 \approx 9 \times 10^{-15}$ A m$^2$. For the dipolar pair, the magnetic moment along the body diagonal makes an angle of 35$^\circ$ with respect to the face diagonal and hence the magnetic moment is given by $\mu_1 = \mu_2 = \mu_{\text{eff}}/2 \cos(35^\circ) \approx 14 \times 10^{-15}$ A m$^2$. The average magnetic moment obtained from two differently assembled pairs of microcubes are given by $\mu = 11.5 \times 10^{-15}$ A m$^2$. This result is very close to the theoretically calculated and experimentally measured value of the bulk sample composed of similar microcubes by an alternating current gradient magnetometer.\cite{30} However, our method is very simple and provides measurement at microscopic level than the conventional method used for bulk sample composed of a very large number of microcubes.

3. Conclusion

Microcubes with homeotropic surface anchoring exhibit mainly three different orientations in a nematic liquid crystal. For majority of the microcubes, the face diagonals of a pair of opposite faces are parallel to the rubbing direction and exhibit quadrupolar interaction. Dipolar structure with a point defect is exhibited by a small number of microcubes for which one of the body diagonals is nearly parallel to the rubbing direction. In a very small fraction of microcubes, two opposite faces are oriented perpendicular to the rubbing direction in which the disclination ring wraps around the four edges of either of the faces. The angle dependence of the elastic interactions is markedly different for all three distinct orientations of the microcubes. Our experiments provide an evidence of defect polymorphism of the microcubes, which was predicted earlier by the computer simulation. With the help of the laser tweezers, we assembled microcubes into various structures, such as highly bent chains, branches, kinks, closed loops, which are not achievable in spherical colloids.\cite{30} The combined effects of particle-shape, anisotropic interaction, and magnetic properties of the microcubes in liquid crystals are effectively used to design diverse building blocks which could be useful for assembling complex, programmable, and magnetically responsive colloidal structures. Our investigations have focused on cubic particles; however, the plethora of faceted colloids accessible promises a wide range of as yet unexplored phenomena and their applications.
4. Experimental Section

Cubic hematite particles ($\alpha$-Fe$_2$O$_3$) were synthesized using sol–gel method.[34,35] In the synthesis, NaOH solution (100 mL, 6 M) was slowly added to 2.0 M FeCl$_3$ solution (100 mL) in a Pyrex bottle and agitated for 15 min. The entire solution was aged for 8 days at 100 °C and washed with milliQ water to obtain the hematite cubes. A thin layer (60 nm) of Silica (SiO$_2$) coating on the cubes was made via an adaption of the Stöber method.[36,37] A smooth layer of silica was grown on to the hematite cube by functionalizing it with polymer polyvinylpyrrolidone (PVP, 40 kg mol$^{-1}$). PVP is a nonionic and amphiphilic polymer that readily adsorbs on a variety of materials. In this study, PVP got adsorbed onto the hematite surface and acted as a coupling agent between the seed particle and the silica coating. PVP also acted as a stabilizing polymer on the silica-coated hematite cube. Approximately 0.5 g of hematite cubes was dispersed in 5 mL of water and the resulting dispersion was mixed with 50 mL of PVP solution. The mixture was stirred for 8 h and then sonicated to ensure the complete dissolution of PVP. Later, ethanol, water, and tetramethylammonium hydroxide (TMAH, 25 wt%) solution were added, followed by dropwise addition of tetraethoxysilane (TEOS). TMAH is a strong base which is used to catalyze the hydrolysis and condensation of TEOS. The resulting solution was washed several times by centrifugation and redispersed in ethanol to obtain silica coated hematite microcubes. Further, the silica coated microcubes were treated with $N,N$-dimethyl-N-octadecyl-3 aminopropyl-trimethoxysilyl chloride (DMOAP) to ensure perpendicular or homeotropic anchoring of the liquid crystal molecules on the surface.

In the next step, the microcubes were dispersed (1 wt%) in a room-temperature nematic liquid crystal, pentyl cyanobiphenyl (5CB) by using a vortex mixture and ultra sonicator. The nematic colloid was filled in cells prepared by two parallel glass plates, which were polyimide (AL-1254) coated and baked at 180 °C, followed by a unidirectional rubbing. The nematic director (n) mean molecular orientation) was aligned along the rubbing direction. The cell gap ($\approx$5–8 μm) was maintained by spherical silica spacers mixed with a UV curable optical adhesive (NOA-81). An inverted polarizing optical microscope (Nikon eclipse Ti-U) with a 60 × water immersion objective and a color camera (Nikon DS-Ri2) was used for texture observation and video recording. A first-order waveplate, so-called $\lambda$-plate (530 nm) was used for constructing director field ($\vec{n}$) surrounding the particles. A laser tweezer operating at 1064 nm (Tweez 250si) was built on the inverted microscope. An acousto-optic deflector (AOD) was used for optical trap and hence the particle manipulation. A charge-coupled device (iDs-UI) was used for the video recording of the particle trajectories. A particle tracking program was used off-line for tracking the centers of the particles with an accuracy of 20 nm.

Supporting Information

Supporting Information is available from the Wiley Online Library or from the author.
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Conflict of Interest

The authors declare no conflict of interest.

Keywords

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