The evolution of the brightest cluster galaxies since $z \sim 1$ from the ESO Distant Cluster Survey (EDisCS)

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ABSTRACT

We present $K$-band data for the brightest cluster galaxies (BCGs) from the ESO Distant Cluster Survey (EDisCS). These data are combined with the photometry published by Aragón-Salamanca, Baugh & Kauffmann and a low-redshift comparison sample built from the BCG catalogue of von der Linden et al. BCG luminosities are measured inside a metric circular aperture with 37 kpc diameter. In agreement with previous studies, we find that the $K$-band Hubble diagram for BCGs exhibits very low scatter ($\sim 0.35$) over a redshift range of $0 < z < 1$. The colour and rest-frame $K$-band luminosity evolution of the BCGs are in good agreement with population synthesis models of stellar populations which formed at $z > 2$ and evolved passively thereafter. In contrast with some previous studies, we do not detect any significant change in the stellar mass of the BCG since $z \sim 1$. These results do not seem to depend on the velocity dispersion of the parent cluster. We also find that there is a correlation between the 1D velocity dispersion of the clusters ($\sigma_{cl}$) and the $K$-band luminosity of the BCGs (after correcting for passive-evolution). The clusters with large velocity dispersions, and therefore masses, tend to have brighter BCGs, i.e. BCGs with larger stellar masses. This dependency, although significant, is relatively weak: the stellar mass of the BCGs changes only by $\sim 70$ per cent over a two order of magnitude range in cluster mass. Furthermore, this dependency does not change significantly with redshift. We have compared our observational results with the hierarchical galaxy formation and evolution model predictions of De Lucia & Blaizot. We find that the models predict colours which are in reasonable agreement with the observations because the growth in stellar mass is dominated by the accretion of old stars. However, the stellar mass in the model BCGs grows by a factor of 3–4 since $z = 1$, a growth rate which seems to be ruled out by the observations. The models predict a dependency between the BCG’s stellar mass and the velocity dispersion (mass) of the parent cluster in the same sense as the data, but the dependency is significantly stronger than observed. However, one major difficulty in this comparison is that we have measured magnitudes inside a fixed metric aperture while the models compute total luminosities.

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1 INTRODUCTION

Brightest cluster galaxies (BCGs) form a very special class of galaxy. They lie in local minima of the cluster potential well and are extremely massive and luminous, forming their own luminosity function (Sandage 1976; Dressler 1978; Bernstein & Bhavsar 2001). BCGs have been the focus of many studies (see e.g. Humason, Mayall & Sandage 1956; Sandage 1972; Gunn & Oke 1975; Hoessel, Gunn & Thuan 1980; Oegerle & Hoessel 1991; Nelson et al. 2002) and are well known for the low scatter in their absolute magnitudes (∼0.3 mag; see e.g. Sandage 1988). Early work involving BCGs took advantage of this small scatter in absolute magnitudes, combined with the extreme luminosities of these galaxies, to examine the cosmological bulk flow out to higher redshifts and to try to determine the value of the deceleration parameter q0 using the BCGs as standard candles (e.g. Sandage 1972; Sandage & Hardy 1973; Gunn & Oke 1975; Lauer & Postman 1992). More recent studies of BCGs have focused on unravelling the formation and evolution of these objects in order to place constraints on galaxy formation models. Aragón-Salamanca et al. (1998, hereafter ABK) examined the K-band Hubble diagram for BCGs up to a redshift of ∼1. They found that the BCGs did not exhibit any luminosity evolution over this redshift range, suggesting that the stellar mass of the BCGs had grown by a factor of 2–4 since z ∼ 1, depending on the cosmology assumed. Collins & Mann (1998) and Brough et al. (2002) also studied the K-band Hubble diagram for the BCGs in an X-ray selected cluster sample. These authors found that the amount of stellar mass growth shown by the BCGs was dependent on the X-ray luminosity of the host cluster, with BCGs in high X-ray luminosity clusters showing no mass accretion since z ∼ 1 and BCGs in low X-ray luminosity clusters growing by a factor of ∼4 in this time.

More recently De Lucia & Blaizot (2007) have used a combination of N-body simulations and semi-analytic techniques to study the formation and evolution of BCGs. They find that the formation history of local BCGs is extremely hierarchical, with half the mass of a typical BCG being locked up in a single galaxy after z ∼ 0.5. The stars that make up the BCGs are formed very early in separate, small galaxies which then assimilate over time to form the BCG.

In this paper, we extend the work carried out by ABK, enlarging their high-redshift sample with the BCGs from the ESO Distant Cluster Survey (EDisCS; White et al. 2005). The local comparison sample is also improved using the BCGs from a Sloan Digital Sky Survey (SDSS) based cluster sample (von der Linden et al. 2007). Moreover, additional information such as the velocity dispersions of the host clusters is now included in the analysis. In Section 2, we present the data and describe our main observational results concerning the stellar mass growth of the BCGs, the evolution of their colours and the relationship between the velocity dispersion of the host cluster and the BCG luminosity. Section 3 compares the observational results with the semi-analytic model predictions of De Lucia & Blaizot (2007). Section 4 summarizes our main conclusions. We assume H0 = 71 km s⁻¹ Mpc⁻¹, Ωm = 0.27 and ΩΛ = 0.73 (Spergel et al. 2003) throughout the paper.

2 OBSERVATIONAL RESULTS

2.1 The sample

One part of the data analysed here is taken from the ESO Distant Cluster Survey (EDisCS), presented in detail in White et al. (2005). A brief description is given here for completeness. The candidate clusters for EDisCS were chosen among the highest surface brightness objects in the Las Campanas Distant Cluster Survey (LDCCS) of Gonzalez et al. (2001). Potential cluster candidates were identified in two redshift bins, mid-z clusters (0.45 < zrest < 0.55) and high-z clusters (0.75 < zrest < 0.85), where zrest is the estimated cluster redshift based on the magnitude of the putative BCG (see Gonzalez et al. 2001 for details). The potential clusters were checked carefully to ensure the detection appeared reliable and deep optical and near-infrared (near-IR) photometry was taken for 20 fields with confirmed cluster candidates. The optical photometry was taken using FORS2 at the Very Large Telescope (VLT) in direct imaging mode. The mid-z clusters were imaged in the B, V and I bands, the high-z clusters in the V, R and I bands. Typical integration times for the optical data were 45 min for the mid-z clusters and 120 min for the high-z clusters. The near-IR J and K photometry was obtained using SOFI at the New Technology Telescope (NTT) (Aragón-Salamanca et al., in preparation). Two fields were not imaged due to bad weather and a further field was rejected as its spectroscopic redshift histogram suggested the cluster was more likely to be a chance superposition of objects spread out over a range of redshift. However, confirmation spectroscopy with FORS2 at the VLT showed that several of the confirmed fields were found to contain multiple clusters at different redshifts, which compensated for the loss of the other three fields (Gonzalez et al. 2002; White et al. 2005). The EDisCS sample considered here contains K-band data for a total of 21 BCGs spread over a redshift range of approximately 0.4 to 0.96. (see Table 1). A minimum of 150 min of integration in the K band was obtained for the mid-z clusters and a minimum of 300 min for the high z ones. Hubble Space Telescope/Advanced Camera for Surveys (HST/ACS) data were also obtained for the 10 highest redshift clusters. Typical random errors for the ground-based photometry are ∼0.007 mag. Errors in the photometric zero-points are ∼0.02 mag. The EDisCS BCGs were identified by examining each cluster individually and choosing the most suitable galaxy in each case, taking into account redshift, brightness and location of surface density peak. Further information regarding the EDisCS photometry and BCG selection is presented in White et al. (2005).

In addition to the EDisCS BCGs, we make use of a sample of local BCGs studied in von der Linden et al. (2007). Only a brief description of how these BCGs were selected is included here. For a more detailed account, see von der Linden et al. (2007). The starting point of this sample was the C4 catalogue (Miller et al. 2005) of clusters in the SDSS (York et al. 2000; Stoughton et al. 2002). However, due to fiber collisions in the SDSS (no two fibers can be placed within 5 arcsec of each other), about a third of the BCGs are missed by the C4 algorithm, which is based on the spectroscopic data alone. A semi-automatic algorithm to identify the brightest, central galaxy of these clusters is presented in detail in von der Linden et al. (2007). Furthermore, an iterative algorithm is used to
determine the redshift $z$, velocity dispersion $\sigma_z$, and virial radius $R_{200}$ from cluster members within 1 $R_{200}$ from the BCG and within $\pm 3\sigma_z$ of the cluster redshift. The final cluster sample contains 625 groups and clusters. Of their BCGs, 604 are found in the 2MASS Extended Source Catalogue (2MASSX; Skrutskie et al. 2006). Further cuts to the local sample during the process of obtaining reliable $K$-band aperture magnitudes (see Section 2.2) reduced the total number of SDSS/2MASS BCGs to 598, covering a redshift range 0.02 $\leq z < 0.10$. These galaxies will be used in the following sections to build a low-redshift sample for comparison, as closely as possible, our high redshift one.

We also combine the EDisCS and SDSS/2MASS data with the photometry published by ABK. We refer the reader to the original paper for a description of their data. ABK provide $K$-band photometry taken in circular apertures of increasing radius (5, 7, 10, 15, 20, 25, 30, 40, 50, and 70 arcsec). The maximum aperture for which a magnitude was available varied from object to object. These aperture magnitudes were then interpolated to estimate the value corresponding to a physical aperture of 37 kpc at the redshift of each BCG. Unfortunately, for six of the SDSS BCGs the required aperture was larger than the maximum aperture that was available from the 2MASSX database. For these objects, it would have been necessary to extrapolate to estimate the required aperture magnitudes. Rather than using uncertain extrapolated magnitudes, we decided to discard these objects, leaving a final sample of 598 SDSS/2MASS BCGs. Simple statistical tests show that these galaxies represent a random subsample of the original SDSS/2MASS BCG sample, unbiased with respect to their redshift distribution, velocity dispersion or luminosity. Galactic extinction corrections were applied to these objects in the same way as for the EDisCS BCGs. The correction was, in general, small (typically $\Delta K < 0.01$ mag). A $k$-correction was also applied to the data as before.

Note that both the 2MASS and the EDisCS photometric data are in the $K_s$ system, while the ABK data are in the United Kingdom Infrared Telescope (UKIRT) $K$ system. However, the differences between the photometric systems are $\leq 0.01$ mag and thus negligible.1

In Section 2.4, we will see that the luminosity of the BCG depends significantly on the velocity dispersion ($\sigma_z$) of the parent cluster. Thus, in order to make meaningful comparisons between the low- and high-redshift BCGs, the velocity dispersions of the cluster samples need to be reasonably well matched. The top panel of Fig. 1 shows that the SDSS/2MASS sample contains a much larger proportion of low $\sigma_z$ clusters than the high-$z$ sample, thus a direct comparison cannot be made. However, given the number of clusters in the SDSS/2MASS sample, it is possible to build reasonably large subsamples of low-$z$ clusters with $\sigma_z$ distributions that are well matched to that of the high-$z$ sample. A set of 1000 local cluster subsamples, each with a $\sigma_z$ distribution matched to our high-$z$ sample, was built by randomly selecting SDSS/2MASS clusters in the right proportion. Each of these $\sigma_z$-matched subsamples contains 50 SDSS BCGs. A typical realization is shown in the bottom panel of Fig. 1. In this sample matching process, we did not take into account the redshift evolution of $\sigma_z$ because such an approach

### Table 1. Corrected rest-frame $K$-band magnitudes for the EDisCS BCGs.

| Cluster | BCG ID         | $z_\ell$ | $K_0$ (Col $km^{-1}$) |
|---------|----------------|----------|-----------------------|
| cl1103−1139a | EDCSNJ1301351−1138356 | 0.3969 | 391±6 |
| cl1202−1224 | EDCSNJ1202433−1224301 | 0.4240 | 518±10 |
| cl1037−1243a | EDCSNJ1037523−1244400 | 0.4252 | 537±16 |
| cl1059−1253 | EDCSNJ1059071−1253153 | 0.4564 | 590±25 |
| cl1018−1211 | EDCSNJ1018467−1211527 | 0.4734 | 486±59 |
| cl1138−11133 | EDCSNJ1138103−1113379 | 0.4796 | 732±76 |
| cl1301−1139 | EDCSNJ1301402−1139229 | 0.4828 | 687±81 |
| cl1420−1236 | EDCSNJ1420201−1236297 | 0.4962 | 218±43 |
| cl1411−1148 | EDCSNJ1410427−1148287 | 0.5195 | 710±125 |
| cl1232−1250 | EDCSNJ1232303−1250364 | 0.5143 | 1080±119 |
| cl1037−1243 | EDCSNJ1037514−1243266 | 0.5783 | 319±53 |
| cl1353−1137 | EDCSNJ1353017−1137285 | 0.5882 | 666±156 |
| cl1103−1245a | EDCSNJ1103349−1246462 | 0.6261 | 336±56 |
| cl1127−1138 | EDCSNJ1127589−1131535 | 0.6357 | 574±72 |
| cl1054−1146 | EDCSNJ1054244−1146194 | 0.6972 | 589±78 |
| cl1103−1245b | EDCSNJ1103365−1244223 | 0.7031 | 252±56 |
| cl1040−1155 | EDCSNJ1040403−1156042 | 0.7043 | 418±55 |
| cl1061−1245 | EDCSNJ1054435−1245519 | 0.7408 | 504±113 |
| cl1354−1230 | EDCSNJ1354098−1231015 | 0.7620 | 648±110 |
| cl1216−1201 | EDCSNJ1216453−1201176 | 0.7943 | 1018±77 |
| cl1103−1245 | EDCSNJ1103434−1245341 | 0.9586 | 534±120 |

1Halliday et al. (2004) and Milvang-Jensen et al. (2008)
would have been model dependent. However, the expected evolution is small enough (e.g. Poggianti et al. 2006) and the dependence of the BCG’s luminosity on σ_v weak enough (cf. Section 2.4) that our conclusions would not change if we had taken such evolution into account.

In the analysis described below, we carried out comparisons between the high-z sample and the 1000 realizations of the low-z σ_v matched sample. The quantitative results we quote always refer to the mean of all these comparisons. For display purposes, and for the sake of clarity, we sometimes only plot the points corresponding to the mean of all these comparisons. This is in agreement with the observed colour evolution of these objects, which suggests that their stars were formed at a redshift z ≈ 2 and then evolved passively (see Section 2.3).

If the stellar populations of these objects are passively evolving, their colour evolution suggests (Section 2.3), the observed luminosity evolution can be used to place limits to the amount of growth in the stellar mass of the BCGs. Following the method of ABK, we parametrize the stellar mass evolution as $M_{\star}(z) = M_{\star}(0) \times (1 + z)^{\gamma}$. Least-squares fits to the data points in the bottom panels of Fig. 2 give the following results:

$z_{\text{form}} = 2 \quad \gamma = -0.3 \pm 0.2,$

$z_{\text{form}} = 5 \quad \gamma = +0.1 \pm 0.2.$

This means that we do not detect any significant change in the stellar mass of these objects. Our data are compatible with zero growth. Formally, the derived γ values and their associated errors imply that, if the stellar populations in these galaxies formed at $z_{\text{form}} = 2$, the stellar mass cannot have grown by more than a factor of 1.9 between $z = 1$ and 0 (3σ upper limit). For $z_{\text{form}} = 5$, the upper limit reduces to a factor of 1.4 (i.e. only 40 per cent). This contrasts with the results obtained by ABK, who suggested stellar mass growths for the BCGs of factors between 2 and 4 since $z \sim 1$. As mentioned above, this difference is mainly due to their low-z normalization. We compare the observed mass growth with the results from semi-analytic models in Section 3.

Collins & Mann (1998) and Brough et al. (2002) found that the amount of stellar mass growth shown by the BCGs could be dependent on the X-ray luminosity of the host cluster, with BCGs in high X-ray luminosity clusters showing little or no stellar mass growth since $z \sim 1$, while BCGs in low X-ray luminosity clusters exhibit a large variation in their stellar mass growth, from clusters showing no growth to a few growing by factors of up to $\sim 4$. As discussed...
Figure 2. Top plot: the apparent rest-frame $K$-band magnitudes versus redshift for the BCGs. The EDisCS points are shown as plus signs, the data from ABK are represented by circles and the galaxies in one of the SDSS/2MASS $\sigma_{cl}$-matched subsamples is shown as crosses. This SDSS/2MASS subsample has properties close to the mean of the 1000 realizations. Small dots correspond to the complete SDSS/2MASS BCG sample, shown here for comparison (see the text for details). The magnitudes have been measured in a fixed metric aperture of 37 kpc. The solid line shows the no-evolution prediction, and the dashed and dotted lines show the predicted evolution for passively evolving stellar populations formed at redshifts of 2 and 5, respectively. The model lines are normalized at low $z$ to the mean of the 1000 $\sigma_{cl}$-matched SDSS/2MASS subsamples. Bottom plot: the top panel shows the data with the no-evolution prediction subtracted (symbols as above). The middle and bottom panels show, respectively, the data after subtracting the passive-evolution predictions for $z_{\text{form}} = 2$ and 5. The dashed line in each panel indicates the average least-squares fits to each of the 1000 low-$z$ subsamples plus the EDisCS and ABK BCGs.

in Section 2.4, the cluster X-ray luminosity and velocity dispersion $\sigma_{cl}$ can be taken as proxies for cluster mass. If we divide our low- and high-$z$ cluster samples into two equal subsamples, one with $\sigma_{cl} \leq 654$ km s$^{-1}$ and the other with $\sigma_{cl} > 654$ km s$^{-1}$, we find that the inferred stellar mass growth does not seem to depend on $\sigma_{cl}$: the stellar mass of the BCGs seems to have remained roughly constant for both subsamples (albeit, with weaker formal limits given the smaller sample sizes). This is shown in Fig. 3, which presents again the lower panels of Fig. 2 with the data split into high- and low-$\sigma_{cl}$ subsamples. There is no significant difference in the luminosity evolution rate of the two $\sigma_{cl}$ subsamples. However, there is clearly an offset between the lines of best fit in each panel of Fig. 3, with the high-$\sigma_{cl}$ sample being brighter in each case. This implies a significant dependence of the luminosity of the BCG on cluster velocity dispersion, as discussed in Section 2.4.

To test whether our conclusions depend strongly on the choice of galaxy evolution models, we have recalculated the expected passive $K$-band luminosity evolution (cf. Fig. 2) using the models of Maraston et al. (2006). Since these models use a very different prescription for TP–AGB stars, the near-IR luminosity evolution is significantly different from that of Bruzual & Charlot (2003) for stellar populations with ages $\sim 0.5$–1 Gyr. However, for the range of ages relevant to our analysis (2.6–12.5 Gyr), the model predictions agree within $\sim 0.1$ mag for a given metallicity and IMF. We are thus confident that the conclusions of this section are reasonably model independent.

2.3 Colours

Fig. 4 shows the observed frame $V - I$ and $I - K$ colours for the EDisCS and SDSS/2MASS BCGs, plotted as a function of redshift. For the EDisCS BCGs, a 2 arcsec radius circular aperture was used to measure the colours. This aperture is large enough to sample a significant fraction of the BCG’s light, while keeping sky-subtraction errors small. The 2 arcsec radius at the average redshift of the EDisCS BCGs ($\sim 0.6$) corresponds to an aperture of radius $\sim 10$ arcsec at the average redshift of the SDSS BCGs ($\sim 0.07$). Optical and near-IR photometry for the SDSS/2MASS sample was measured inside circular apertures with 10 arcsec radius, and transformed into the $VIK$ system following Blanton & Roweis (2007).

The colours were corrected for galactic extinction but not $k$-corrected. The lines shown in Fig. 4 are predictions created using the population synthesis code of Bruzual & Charlot (2003). The solid lines represent the expected colour evolution of a stellar population with solar metallicity and a Salpeter (1955) IMF which formed in an instantaneous burst at $z = 2$ and then evolved passively. The dotted and dashed lines show the expected evolution for similar stellar populations that formed at $z = 5$ and 1, respectively. It is clear from

3 Measuring galaxy colours inside the metric aperture used in Section 2.2 (average radius $\sim 2.5$ arcsec) makes no significant difference to the conclusions of this section.
the BCGs are composed of stellar populations that formed at high-$z$ and have been evolving passively since. Similar conclusions are obtained using the Maraston et al. (2006) models. For the range of ages relevant to $z_{\rm form}$ between 2 and 5, these models predict colours which agree with those of Bruzual & Charlot (2003) within $\lesssim 0.1$ mag. This should be taken as an indication of the typical uncertainties associated with model colours. For that reason, the fact that the $V - I$ BCG colours seem to agree with the $z_{\rm form} = 5$ models while for $I - K$ there is better agreement with $z_{\rm form} = 2$ is not significant. Nevertheless, since the $V$ band samples the rest-frame ultraviolet, a very small amount of recent star formation (say, $\sim 1$ per cent by mass) could easily make the observed $V - I$ colours bluer by $\sim 0.1$ while having negligible effect on $I - K$.

As the metallicity of the BCGs is unknown, the colour evolution predictions were also calculated for a stellar population with approximately double solar metallicity and also approximately half solar metallicity. These predictions were found to lie nowhere near the plotted data points, being far too red and blue, respectively, to reproduce the colour evolution exhibited by the BCGs. This shows that although the colour evolution predictions are sensitive to changes in metallicity, the assumption of approximately solar metallicity is a reasonable one.

2.4 BCG $K$-band luminosity and cluster velocity dispersion

Arguably, the most fundamental property of a cluster is its mass, so it is not unreasonable to expect that the luminosity (and stellar mass) of the BCGs may be related to it. Several observational properties can be used as proxies for the cluster mass, including the cluster X-ray luminosity and temperature and the cluster velocity dispersion $\sigma_{\text{cl}}$. Indeed, Edge & Stewart (1991) found a significant correlation, in a low-$z$ sample, between the optical luminosity of the BCGs and the X-ray luminosity and temperature of the parent clusters in the sense that hotter and more X-ray bright clusters host brighter BCGs.

Velocity dispersions are available for all the EDisCS and SDSS clusters and 10 of the clusters studied by ABK. Columns 4 of Tables 1 and 2 show the velocity dispersions $\sigma_{\text{cl}}$ of the EDisCS and SDSS/2MASS $\sigma_{\text{cl}}$-matched cluster samples. A full description of the calculation of the $\sigma_{\text{cl}}$ values for the SDSS clusters can be found in von der Linden et al. (2007). Information regarding the EDisCS $\sigma_{\text{cl}}$ values can be found in Halliday et al. (2004), Poggianti et al. (2006) and Milvang-Jensen et al. (2008). The velocity dispersions for the ABK clusters are taken from Girardi & Mezzetti (2001) and Lubin, Oke & Postman (2002). Note that in all these studies the cluster velocity dispersions have been determined following very similar methods, and are thus directly comparable.

In order to test for any relationship between the BCG $K$-band luminosity (or stellar mass) and the cluster mass, we have calculated the residuals around the three lines of best fit shown in the bottom three panels of Fig. 2 and plotted them against $\log_{10}(1+z)$ in Fig. 7. This procedure should correct for redshift-related effects. The panels show, from top to bottom, the residuals around the line of best fit after the rest-frame $K$-band magnitudes have been corrected for no-evolution, passive-evolution with $z_{\text{form}} = 2$ and 5, respectively (cf. Fig. 2). The symbols for the EDisCS and the ABK samples are the same as in Fig. 2. As an illustration, we also show (crosses) the BCGs in the SDSS/2MASS $\sigma_{\text{cl}}$-matched subsample whose line of best fit (see below) is closest to the mean of the 1000 subsamples.

There is a clear trend in each panel of Fig. 7 indicating that clusters with large velocity dispersions, and presumably large masses, tend to have brighter BCGs. A Spearman rank correlation coefficient analysis indicates that all these correlations are significant at a level greater than 99.9 per cent.

Fig. 4 that, within the model uncertainties (see below), there is reasonably good agreement between the data and the passive-evolution models with $z_{\text{form}} = 2$ and 5. As expected, the model for $z_{\text{form}} = 1$ does not fit the data at all. The agreement between the colours of the BCGs and the passive-evolution models is a strong indication that the BCGs are composed of stellar populations that formed at $z \gtrsim 2$ and have been evolving passively since. Similar conclusions are obtained using the Maraston et al. (2006) models. For the range of ages relevant to $z_{\text{form}}$ between 2 and 5, these models predict colours which agree with those of Bruzual & Charlot (2003) within $\lesssim 0.1$ mag. This should be taken as an indication of the typical uncertainties associated with model colours. For that reason, the fact that the $V - I$ BCG colours seem to agree with the $z_{\text{form}} = 5$ models while for $I - K$ there is better agreement with $z_{\text{form}} = 2$ is not significant. Nevertheless, since the $V$ band samples the rest-frame ultraviolet, a very small amount of recent star formation (say, $\sim 1$ per cent by mass) could easily make the observed $V - I$ colours bluer by $\sim 0.1$ while having negligible effect on $I - K$.

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There is a clear trend in each panel of Fig. 7 indicating that clusters with large velocity dispersions, and presumably large masses, tend to have brighter BCGs. A Spearman rank correlation coefficient analysis indicates that all these correlations are significant at a level greater than 99.9 per cent.
Table 2. Corrected rest-frame K-band magnitudes for a typical $\sigma_{cl}$-matched SDSS subsample. The properties of this subsample are close to the mean of the 1000 subsamples (see Section 2.4.).

| SDSS BCG ID | $z_{cl}$ | $K_0$ | $\sigma_{cl}(\text{km s}^{-1})^2$ |
|------------|---------|-------|----------------------------------|
| 58772610452550731 | 0.02015 | 8.7 | 502 ± 49 |
| 58772953306931328 | 0.04362 | 12.0 | 264 ± 31 |
| 588015507664928793 | 0.04437 | 10.5 | 933 ± 73 |
| 58772893241042326 | 0.0463 | 11.2 | 556 ± 59 |
| 58772867041822798 | 0.04845 | 11.5 | 570 ± 79 |
| 58848899917610122 | 0.04876 | 10.9 | 211 ± 49 |
| 58772953749852828 | 0.05189 | 11.9 | 547 ± 86 |
| 58772272705263139 | 0.0558 | 10.7 | 903 ± 55 |
| 58772952231944566 | 0.05596 | 12.9 | 685 ± 82 |
| 58773403443718742 | 0.05625 | 12.4 | 915 ± 70 |
| 587730381347195107 | 0.05643 | 11.4 | 441 ± 45 |
| 58772928337535296 | 0.06003 | 11.9 | 506 ± 51 |
| 5877975113029774 | 0.06029 | 11.2 | 512 ± 87 |
| 5877321340350396 | 0.06288 | 11.7 | 613 ± 82 |
| 58773118566884907 | 0.06517 | 11.9 | 1084 ± 113 |
| 588010360151146773 | 0.06901 | 12.2 | 800 ± 57 |
| 58773308182755176 | 0.07017 | 13.0 | 543 ± 94 |
| 587726032259973170 | 0.07104 | 11.6 | 541 ± 92 |
| 58772352591168714 | 0.07267 | 12.1 | 582 ± 100 |
| 58775566021898155 | 0.07371 | 11.4 | 670 ± 77 |
| 587731680111820927 | 0.07587 | 12.5 | 902 ± 96 |
| 58772225698387020 | 0.07618 | 11.5 | 812 ± 48 |
| 58772601668174265 | 0.07739 | 11.8 | 966 ± 60 |
| 58772712807192844 | 0.07868 | 12.8 | 765 ± 97 |
| 587726031184920689 | 0.07919 | 13.1 | 535 ± 59 |
| 587725576423342431 | 0.08012 | 12.0 | 1156 ± 62 |
| 58772601138339907 | 0.08044 | 13.0 | 677 ± 51 |
| 588015508205994134 | 0.08157 | 12.0 | 497 ± 63 |
| 58772550559986848 | 0.08182 | 12.6 | 613 ± 92 |
| 58773081736164713 | 0.08255 | 13.1 | 406 ± 80 |
| 587728677271130340 | 0.08257 | 13.4 | 315 ± 57 |
| 587726032776593461 | 0.08316 | 12.6 | 424 ± 78 |
| 587733080184780480 | 0.08330 | 12.3 | 625 ± 74 |
| 587730816824508498 | 0.08512 | 12.5 | 229 ± 72 |
| 587729782810345782 | 0.08578 | 12.3 | 530 ± 102 |
| 588013381670994051 | 0.08581 | 12.8 | 409 ± 73 |
| 58772975274728348 | 0.08803 | 11.7 | 951 ± 57 |
| 58773341096590314 | 0.08804 | 11.9 | 705 ± 86 |
| 58848899917873272 | 0.08820 | 12.2 | 1020 ± 87 |
| 587728900454678767 | 0.08856 | 11.9 | 708 ± 102 |
| 587733604808548243 | 0.08901 | 13.1 | 556 ± 110 |
| 58773661877335756 | 0.09010 | 12.4 | 794 ± 58 |
| 587722982384438274 | 0.09059 | 12.2 | 748 ± 61 |
| 587726100415774901 | 0.09243 | 12.3 | 513 ± 83 |
| 587735694836039706 | 0.09356 | 13.3 | 554 ± 162 |

Note that the correlations found and their estimated slopes are robust against changes in the way we account for the passive luminosity evolution of the BCGs. The slopes of the $L_{\text{K}} - \sigma_{cl}$ relations are the same for the low- and high-z samples. This seems to indicate that in the range of redshifts explored here the rate of the BCG buildup and that of the cluster is linked in a way that does not depend strongly on cosmic time.

Another interesting result is that, although significant, the dependency of $L_{\text{K}}$ (presumably proportional to the BCG’s stellar mass $M^{\text{BCG}}_{*}$) on $\sigma_{cl}$ is relatively weak. If we assume that the cluster mass $M_{cl}$ is proportional to $R_{200}^3 \sigma_{cl}^2$, where $R_{200}$ is the radius of a sphere with interior mean density 200 times the critical density of the Universe at the cluster redshift. If we also assume that, at a given redshift, $R_{200} \propto \sigma_{cl}$ (Carlberg, Yee & Ellingson 1997; Finn et al. 2005), then $M_{cl} \propto \sigma_{cl}^2$ and $M^{\text{BCG}}_{*} \propto M_{cl}^{0.35}$. Thus, the stellar mass of BCGs changes only by ~70 per cent over a two order of magnitude range in cluster mass. This is not surprising: it has long been known that BCG luminosities measured inside fixed metric apertures provide reasonable standard candles almost independent of the cluster richness (Postman & Lauer 1995).

Very recently, Brough et al. (2008) and Stott et al. (2008) have found similar results for X-ray selected cluster samples.

3 COMPARISON WITH GALAXY FORMATION MODELS

In this section, we compare our empirical results with theoretical predictions from De Lucia & Blaizot (2007). These authors use a combination of large N-body collisionless cosmological simulations and semi-analytic techniques. The semi-analytic models are grafted on to the hierarchical merging trees extracted from the Millennium Simulation (Springel et al. 2005). In this study, we compare our results with two versions of the semi-analytic model which differ for the prescriptions adopted for the supernova feedback. In the following, we will refer as model 1 to a model which employ the same supernova feedback model used in De Lucia et al. (2006) where the ejection rates are computed on the basis of energy conservation.
arguments. We will refer as model 2 to a model which adopts the
same supernovae feedback model as in Croton et al. (2006) where
the ejection rates are proportional to the star formation rate. De
Lucia & Blaizot (2007) have shown that model 1 results in a slower
evolution of the K-band magnitudes as a function of redshift, albeit
producing K-band magnitudes of local BCGs brighter than a factor
of about 0.8 mag with respect to results from model 2.

In order to compare our results to model predictions, we ex-
tracted 90 haloes within the simulation box, uniformly distributed
in log(mass) between $5 \times 10^{12}$ and $5 \times 10^{15} \, M_{\odot}$. We extracted
the haloes from the output of the simulation at $z = 0$ and followed their
history back in time by tracking, at each time, the main progeni-
tor branch defined as in De Lucia & Blaizot (2007). For each SN
feedback model, we have then created tables with rest frame and
observed frame magnitudes in five different bands ($B, V, R, I, J$ and
$K$) for the brightest galaxy in each halo. For each halo, we have
also calculated the 3D and projected velocity dispersions using all
galaxies within $2 \times R_{200}$ at three redshifts ($z = 0.04, 0.36$ and 0.76).
In order to simulate the errors associated with the observed $\sigma_{cl}$ val-
ues, for each halo and each redshift we extracted a random number
of objects, between 20 and 70 from all galaxies within $2 \times R_{200}$ and
computed the 1D velocity dispersion and their confidence lim-
its using the same method that was used to calculate the velocity
dispersions for the EDisCS clusters (Halliday et al. 2004).4 This
method tries to mimic the observational uncertainties in the model
predictions.

When selecting the model cluster sample to compare with obser-
vations, there are two obvious alternatives. First, one could follow
the evolution of the same model clusters, i.e. select clusters at all
redshifts which, at a given redshift (e.g. $z = 0$), have $\sigma_{cl} > \sigma_{lim}$. Sec-
ondly, one could follow similar cluster ‘samples’, i.e. select clusters
at, each redshift, have $\sigma_{cl} > \sigma_{lim}$. Obviously, the first selection
tells us what happens to the same set of galaxies, while the second
one is probably closer to observations since it follows comparable
samples. We will therefore follow the second selection method with
$\sigma_{lim} \simeq 200 \, \text{km s}^{-1}$ (64–70 model clusters, depending on redshift) and
$\sigma_{lim} \simeq 400 \, \text{km s}^{-1}$ (28–45 model clusters, also depending on
redshift), which seem reasonable limits for comparison with our
data set (cf. Fig. 1). Note that the $\sigma_{lim}$ for EDisCS is not well de-
efined since velocity dispersion was not explicitly part of the EDisCS
cluster selection criteria. However, since the results do not depend
on the precise value of this limit, the choice is not critical.

Fig. 5 shows the model $\sigma_{cl}$ distribution at each redshift bin ob-
tained using this selection technique. Although the model $\sigma_{cl}$ values
were not explicitly matched in each redshift bin, as was done for
the observational data, their distributions are well matched at all
redshifts considered. Moreover, they are also well matched to the
$\sigma_{cl}$ values of the observational data (cf. Fig. 1).

The first result of the comparison is that the colours of the model
galaxies are similar to the observed ones for model 1, i.e. close to
those of passively evolving stellar populations formed early. This
suggests that even if the buildup of the galaxies’ stellar mass is
gradual, this growth is dominated by the accretion of old stellar
populations rather than by new star formation. Model 2 predicts
somewhat bluer colours.

Both models 1 and 2 predict a growth in stellar mass that is
significantly stronger than observed: the stellar mass of model BCGs
grows by about a factor of $\sim 3–4$ between $z \sim 1$ and 0, while the
observations are compatible with no growth at all and seem to rule
out a factor of 2 growth since $z \sim 1$ (cf. Section 2.2). The stellar mass
growth in the models does not depend strongly on which feedback
method is used, although it is marginally stronger in model 2. The
stellar mass growth is also quite insensitive to the value of $\sigma_{lim}$,
which agrees with the observed independence of the stellar mass
growth on $\sigma_{cl}$. These results are illustrated in Fig. 6.
Brightest cluster galaxies since $z \sim 1$

Figure 7. Plots of the residuals from the lines of best fit in Fig. 2 versus $\log_{10}(\sigma_{cl})$. The top panel shows the residuals after subtracting the no-evolution prediction. The middle and bottom panels show the same but for the passive-evolution models with $z_{\text{form}} = 2$ and 5, respectively. The EDisCS clusters have been plotted as plus signs, the points from the ABK sample for which we have velocity dispersions are plotted as circles and the data for a typical SDSS/2MASS $\sigma_{cl}$-matched subsample have been plotted as crosses. The SDSS/2MASS subsample shown has a slope very close to the mean slope of all 1000 subsamples (see the text for details). The dotted lines represent the least-squares fits to the EDisCS/ABK data and the solid lines represent the average least-squares fits to the 1000 SDSS/2MASS subsamples. The dashed lines represent the average slope predicted by the semi-analytic models described in the text.

Finally, we compare the observed dependency of the BCGs’ corrected $K$-band luminosity (or stellar mass) with the cluster velocity dispersion (cf. Section 2.4). For model 1, regardless of the exact value of $\sigma_{\text{lim}}$, the models predict, at all the redshifts considered, $L_K \propto \sigma_{cl}^{1.4}$ or $M_{\text{BCG}} \propto M_{cl}^{0.2}$. Model 2 predicts $L_K \propto \sigma_{cl}^{1.2}$ or $M_{\text{BCG}} \propto M_{cl}^{0.4}$. The data suggest a much weaker dependency of the stellar mass on the cluster velocity dispersion or mass. That is clearly shown in Fig. 7: the dashed line represents the average slope from the model predictions, which is significantly steeper than the data.

One major caveat in the comparison of our observations with the semi-analytical model results is that we have used magnitudes measured inside a fixed metric aperture while the models compute total magnitudes. Observationally, it is very difficult (virtually impossible) to measure accurate total magnitudes for the BCGs (see e.g. Gonzalez, Zabludoff & Zaritsky 2005). Indeed, it is not even clear whether one should include the intracluster light (ICL) as part of the BCG’s luminosity (Gonzalez, Zaritsky & Zabludoff 2007). A 37 kpc diameter aperture encompasses only 25–50 per cent of the total light contained in the BCG and ICL (Gonzalez, Zaritsky and Zabludoff, private communication). Interestingly, using the $I$-band data published by these authors we find that although their 37 kpc aperture magnitudes show a dependency with $\sigma_{cl}$ compatible with our measurements, their total BCG+ICL luminosities show a significantly steeper dependence ($L_{\text{BCG+ICL}} \propto \sigma_{cl}^{0.6}$). Although the slope is still considerably shallower than the model predictions, this could explain at least part of the disagreement between models and observations. Note, however, that the scatter is large and their sample relatively small.

On the other hand, the models do not have spatial information regarding the distribution of the BCG light, so aperture magnitudes cannot be calculated. It is also not clear whether the luminosities of the model BCGs contain some of what, observationally, we could call intracluster light. The luminosity of the model BCG includes the stars formed in the central cluster halo and the stars formed in galaxies that merged with the central galaxy, but not stars stripped from other cluster galaxies due to tidal and ‘harassment’ effects, since these are not modelled. Therefore, any discrepancy (and/or agreement) found in the behaviour of the observed and model BCGs should be taken with caution, since not all the physical effects which potentially contribute to the growth of the BCGs are taken into account.

A possible way of reconciling our observations and the model predictions could be that, if there is a large stellar mass growth in BCGs (e.g. a factor of 4 since $z \sim 1$), these stars could lie outside of the 37 kpc apertures we have used in our measurements. In that case, such a growth would really represent the growth of the intracluster component rather than the central BCG. How such growth would depend on the cluster properties is difficult to predict, but it is clear that the intracluster component could play a very important role in the formation and evolution of clusters (see e.g. Lin & Mohr 2004).
For recent theoretical studies of the formation of the intracluster light, see Monaco et al. (2006) and Conroy, Wechsler & Kravtsov (2007).

4 CONCLUSIONS

In this paper, we present new $K$-band data for 21 brightest cluster galaxies (BCGs) from the ESO Distant Cluster Survey (EDisCS). Combining these data with the photometry published by ABK, we have built a sample of 42 BCGs with good quality near-IR photometry in the $0.2 < z < 1$ redshift range. We have also put together a low-redshift ($z = 0.07$) comparison sample from the BCG catalogue of von der Linden et al. (2007) for which optical and near-IR photometry is available from the SDSS and 2MASS. By comparing the properties of the BCGs in the low- and high-$z$ data sets and those of their parent clusters, we have carried out a detailed study of the evolution of these galaxies. Since, as we demonstrate, the properties of the BCGs depend upon the velocity dispersion of the clusters) and the $K$-band luminosity of the BCGs (after correcting for passive-evolution). Clusters with large velocity dispersion of the BCGs with larger stellar masses. This dependency, although significant, is relatively weak: the stellar mass of the BCGs changes by a factor of 1.9 between $z = 1$ and 0 (3σ upper limit). This result does not seem to depend on the velocity dispersion of the parent cluster.

(i) In agreement with previous studies, we find that the $K$-band Hubble diagram for BCGs exhibits very low scatter ($<0.35$ mag) over a redshift range of $0 < z < 1$.

(ii) The colour evolution of BCGs as a function of redshift shows good agreement with population synthesis models of stellar populations that formed at $z > 2$ and evolved passively thereafter.

(iii) In contrast with some previous studies (e.g. ABK), we find that the rest-frame $K$-band luminosity evolution of the BCGs is also well reproduced by passive-evolution models. The main reason for this discrepancy is the use of a different, hopefully more accurate, low-redshift comparison sample with well-matched $\sigma_{\text{1D}}$ distribution.

(iv) The agreement of the observations with passive luminosity evolution models means that we do not detect any significant change in the stellar mass of the BCG since $z \sim 1$. Formally, we rule out a growth in the stellar mass larger than a factor of 1.9 between $z = 1$ and 0 (3σ upper limit). This result does not seem to depend on the velocity dispersion of the parent cluster.

(v) We find that there is a correlation between $\sigma_{\text{1D}}$ (the 1D velocity dispersion of the clusters) and the $K$-band luminosity of the BCGs (after correcting for passive-evolution). Clusters with large velocity dispersions, and therefore masses, tend to have brighter BCGs, i.e. BCGs with larger stellar masses. This dependency, although significant, is relatively weak: the stellar mass of the BCGs changes by a factor of 1.9 between $z = 1$ and 0 (3σ upper limit). This result does not seem to depend on the velocity dispersion of the parent cluster.

We have compared our observational results with the hierarchical galaxy formation and evolution model predictions of De Lucia & Blaizot (2007). One major difficulty in this comparison is that we have measured magnitudes inside a fixed metric aperture while the models compute total luminosities. We find that the models predict colours which are in reasonable agreement with the observations because the growth in stellar mass is dominated by the accretion of old stars. However, the stellar mass in the model BCGs grows by a factor of $\sim 3$–4 since $z = 1$, a growth rate which seems to be ruled out by the observations. The models predict a dependency between the BCG’s stellar mass and the velocity dispersion (mass) of the parent cluster in the same sense as the data, but the dependency is significantly stronger than observed. It therefore seems as if building realistic BCGs is another challenge for this kind of models, indicating that the underlying physics is far from being completely understood.

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