THE ROLE OF TORSIONAL ALFVÉN WAVES IN CORONAL HEATING

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Received 2009 September 28; accepted 2010 February 3; published 2010 March 3

ABSTRACT

In the context of coronal heating, among the zoo of magnetohydrodynamic (MHD) waves that exist in the solar atmosphere, Alfvén waves receive special attention. Indeed, these waves constitute an attractive heating agent due to their ability to carry over the many different layers of the solar atmosphere sufficient energy to heat and maintain a corona. However, due to their incompressible nature these waves need a mechanism such as mode conversion (leading to shock heating), phase mixing, resonant absorption, or turbulent cascade in order to heat the plasma. Furthermore, their incompressibility makes their detection in the solar atmosphere very difficult. New observations with polarimetric, spectroscopic, and imaging instruments such as those on board the Japanese satellite Hinode, or the Crisp spectropolarimeter of the Swedish Solar Telescope or the Coronal Multi-channel Polarimeter, are bringing strong evidence for the existence of energetic Alfvén waves in the solar corona. In order to assess the role of Alfvén waves in coronal heating, in this work we model a magnetic flux tube being subject to Alfvén wave heating through the mode conversion mechanism. Using a 1.5 dimensional MHD code, we carry out a parameter survey varying the magnetic flux tube geometry (length and expansion), the photospheric magnetic field, the photospheric velocity amplitudes, and the nature of the waves (monochromatic or white-noise spectrum). The regimes under which Alfvén wave heating produces hot and stable coronae are found to be rather narrow. Independently of the photospheric wave amplitude and magnetic field, a corona can be produced and maintained only for long (>80 Mm) and thick (area ratio between the photosphere and corona >500) loops. Above a critical value of the photospheric velocity amplitude (generally a few km s\textsuperscript{-1}) the corona can no longer be maintained over extended periods of time and collapses due to the large momentum of the waves. These results establish several constraints on Alfvén wave heating as a coronal heating mechanism, especially for active region loops.

Key words: magnetohydrodynamics (MHD) -- Sun: corona -- Sun: flares -- waves

Online-only material: color figure

1. INTRODUCTION

New observations from polarimetric, spectroscopic, and imaging instruments are revealing a corona permeated with waves. Compressive modes such as the slow and fast magnetohydrodynamic (MHD) modes have a long chapter in observational history (see reviews by Nakariakov & Verwichte 2005; Banerjee et al. 2007; Ruderman & Erdélyi 2009; Taroyan & Erdélyi 2009). Only recently, the development of high-resolution instruments has brought strong evidence for the existence of the third MHD mode, the Alfvén mode, in the solar atmosphere. In the majority of the observational reports of Alfvén waves, ambiguity exists and the waves can be interpreted as trapped modes, fast and slow kink waves. De Pontieu et al. (2007) reported transversal displacements of spicules from observations in the Ca\textsc{ii} H line (3968 Å) with a broadband filter of the Hinode/SOT. The wavelengths of these chromospheric agents were estimated to be longer than 20,000 km, with periods between 100 s and 500 s and speeds of at least 50–200 km s\textsuperscript{-1}. In the absence of a stable waveguide, they interpreted the swaying of the spicules as a result of upward propagating Alfvén waves. However, it was pointed out by Erdélyi & Fedun (2007) that these waves were likely to be kink oscillations, due to the displacement of the axis of symmetry of the flux tube caused by the later. Using the Coronal Multi-channel Polarimeter (CoMP), Tomczyk et al. (2007) analyzed properties of infrared coronal emission line Fe\textsc{xiii} (1074.7 nm) across a large field of view with short integration times. Waves propagating along magnetic field lines with ubiquitous quasi-periodic fluctuations in velocity with periods between 200 s and 400 s (power peak at 5 minutes) and negligible intensity variations were reported. Wavelengths and phase speeds were estimated to be higher than 250 Mm and 1 Mm s\textsuperscript{-1}, respectively. In this work, it was suggested that these waves were Alfvén waves probably being generated in the chromospheric network from mode conversion of $p$-modes propagating from the photosphere (hence explaining the peak in the power spectrum of the waves). On the other hand, Erdélyi & Fedun (2007) and Van Doorsselaere et al. (2008) argued that an interpretation in terms of fast kink waves was more appropriate due mainly to the observed collective behavior which should be absent in the case of Alfvén waves. Though compressible waves, it was argued that kink waves would appear incompressible in the corona for an instrument such as CoMP due to the very small variation in intensity they produce.

The difficulty in detecting the Alfvén wave is due in part to its incompressible nature. Being only a transverse disturbance in the magnetic field, it is practically invisible to imaging instruments, unless the structure of propagation is displaced periodically from the line of sight (Williams 2004). Also, due to the large wavelengths (a few megameters) and short periods (a few minutes) that may be involved in the corona, a large field of view, short integration time, and proper resolution are needed for their detection in the corona. With polarimeters and spectrographs, however, Alfvén waves are more easily

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For instance, assuming an Alfvén speed of 10 km s\(^{-1}\), expanding they reported a canopy-like structure with magnetic fields extending from high to low β plasmas. This large expansion is crucial for Alfvén wave heating theories. For instance, assuming an Alfvén speed of 10 km s\(^{-1}\) in the upper photosphere/lower chromosphere and a period of 100 s (a value in the lower range of periods reported in the works cited above), we obtain a wavelength of 1000 km for Alfvén waves propagating from the photosphere, matching the distance of large expansion of the flux tubes. Moreover, the height in the atmosphere where this takes place is the region of transition from high-β to low-β plasmas. We thus have ideal conditions for mode conversion. Trapped modes will thus exchange their energy and a wide range of waves with different characteristics are likely to issue from this region.

The large emphasis that has been put on the search for Alfvén waves in the solar corona is largely due to their connection with coronal heating. Theoretically, they can be easily generated in the photosphere by the constant turbulent convective motions, which inputs large amounts of energy into the waves (Muller et al. 1994; Choudhuri et al. 1993). Having magnetic tension as its restoring force, the Alfvén wave is less affected by the large transition region gradients with respect to other modes. Also, when traveling along thin magnetic flux tubes they are cutoff free since they are not coupled to gravity (Musiela et al. 2007). Alfvén waves generated in the photosphere are thus able to carry sufficient energy into the corona to compensate the losses due to radiation and conduction, and, if given a suitable dissipation mechanism, heat the plasma to the high million degree coronal temperature (Uchida & Kaburaki 1974; Wentzel 1974; Hollweg et al. 1982; Poedts et al. 1989; Ruderman et al. 1997; Kudoh & Shibata 1999) and power the solar wind (Suzuki & Inutsuka 2006; Cranmer et al. 2007).

Another possible generation mechanism for Alfvén waves is through magnetic reconnection. The amount of energy imparted to these waves during the reconnection process may depend on the location in the atmosphere of the event and is a subject of controversy. Parker (1991) suggested a model in which 20% of the energy released by reconnection events in the solar corona is transferred as a form of Alfvén wave. Yokoyama (1998) studied the problem simulating reconnection in the corona, and found that less than 10% of the total released energy goes into Alfvén waves. This result is similar to the two-dimensional (2D) simulation results of photospheric reconnection by Takeuchi & Shibata (2001), in which it is shown that the energy flux carried by the slow magnetoacoustic waves is i order of magnitude higher than the energy flux carried by Alfvén waves. On the other hand, recent simulations by Kigyre et al. (2010) show that the fraction of Alfvén wave energy flux in the total released magnetic energy during reconnection in low β plasmas may be significant (more than 50%). Since the observed ubiquitous intensity bursts (nanoflares) are thought to play an important role in the heating of the corona (Hudson 1991) and since they are generally assumed to be a signature of magnetic reconnection, it is then crucial to determine the energy going into the Alfvén waves during the reconnection process. Moreover, it is possible that the observed nanoflares themselves are a consequence of Alfvén wave heating as proposed by Moriyasu et al. (2004). In that work, the resulting intensity bursts producing the nanoflares are created by Alfvén waves, which first convert to longitudinal modes which steepen into shocks and heat the plasma. This model was further developed by Antolin et al. (2008, hereafter Paper 1) and Antolin et al. (2009), where it was shown that the frequency of the resulting heating events from Alfvén waves followed a power-law distribution. It was further shown that Alfvén wave heating could be differentiated from nanoflare-reconnection heating during observations through a series of signatures (see also Taroyan 2008; Taroyan & Erdélyi 2009). For instance, Alfvén waves lead to a dynamic, uniformly heated corona with steep power-law indices (issuing from statistics of heating events) while nanoflare-reconnection heating leads to lower dynamics (unless catastrophic cooling takes place in the case of footprint concentrated heating) and shallow power laws.

The main problem faced by Alfvén wave heating is to find a suitable dissipation mechanism. Being an incompressible wave it must rely on a mechanism by which the magnetic energy can be converted into heat. Several dissipation mechanisms have been proposed, such as parametric decay (Goldstein 1978; Terasawa et al. 1986), mode conversion (Hollweg et al. 1982; Kudoh & Shibata 1999; Moriyasu et al. 2004), phase mixing (Heyvaerts & Priest 1983; Ofman & Aschwanden 2002), or resonant absorption (Ionson 1978; Hollweg 1984; Poedts et al. 1989; Erdélyi & Goossens 1995). The main difficulty lies in dissipating sufficient amounts of energy in the correct time and space scales. For more discussion regarding this issue the reader can consult, for instance, Klimchuk (2006), Erdélyi & Ballai (2007), and Aschwanden (2004).

Due to the observed increasing importance of Alfvén waves in the solar atmosphere, in this work we address the subject of coronal heating by Alfvén waves in which mode conversion and parametric decay are taken as dissipation mechanisms. We concentrate on the heating of closed magnetic structures which populate the solar atmosphere, such as coronal loops, and analyze the efficiency of this heating model by carrying out a parametric space survey. We take a 1.5 dimensional (1.5D) model and we consider different photospheric drivers (a random driver creating a white-noise spectrum, or a monochromatic driver in which several periods are tested), vary the photospheric magnetic field, the loop expansion from the photosphere to the corona and the loop length, and determine the regimes for which Alfvén wave heating plays an important role in coronal heating. The paper is organized as follows. In Section 2, we set up the loop geometries and define the equations. As in Antolin et al. (2008), the loops are modeled with a 1.5D MHD code including thermal conduction and radiative cooling. In Section 3, we analyze the effect of varying the parameters on the thermodynamic structure of the loop. Further discussion and conclusions are presented in Section 4.
2. ALFVÉN WAVE MODEL

2.1. Parameter Space

The parametric survey in this work involves parameters changing the geometry of the loop, such as the loop’s length and its expansion from the photosphere to the corona. We consider lengths of 100 Mm, 80 Mm, and 60 Mm, leading to lengths of the corona of roughly 70 Mm, 50 Mm, and 20 Mm, respectively, which are typical lengths for coronal loops.

Due to the passage from gas pressure-dominated (high $\beta$) to magnetic pressure-dominated (low $\beta$) plasmas as we move to higher layers from the photosphere, magnetic flux tubes are expected to expand in the photosphere and chromosphere, forming the so-called magnetic canopy, and have a roughly constant cross-sectional area in the corona (Aschwanden & Nightingale 2005). The loop expansion is a parameter influencing considerably the behavior of the waves as they propagate through the structure. Also, refraction of the fast MHD mode can easily occur, as fast MHD waves will always tend to follow the regions of higher $\beta$ plasma. Hence, expansion can determine not only the properties but also the nature of the waves that propagate along the magnetic field. Here we consider different expansions of the loop displaying a cross-sectional area ratio between the photosphere and the corona of 1000, 600, and 500.

Apart from the previous geometrical parameters, we also consider different photospheric magnetic field strengths. Observations have shown the existence of kilogauss photospheric flux tubes all over the solar surface. Values have been reported ranging from below 1 kG to above 2 kG with a mean around 1.5 kG (Solanki 1993). Here we survey different values for the photospheric magnetic field at the footpoint of the loop, namely, 2.3 kG, 1.5 kG, and 1 kG, and investigate the influence on the thermodynamics of the loop.

Another parameter we consider concerns the photospheric driver generating the Alfvén waves. So far, the few observations of Alfvén waves in the solar atmosphere seem to indicate a broad spectrum range roughly between 100 s and 500 s (see the introduction) with a power peak close to the 5 minute power peak. This may indicate that Alfvén waves share with the $p$-modes the photosphere as generation site. The waves could be a consequence of the constant buffeting of the magnetic field by convection, or possibly, photospheric magnetic reconnection. If, instead, Alfvén waves are primarily generated by magnetic reconnection higher up in the atmosphere, it is difficult to explain the observed common power peak. A possible scenario could be one in which $p$-modes trigger magnetic reconnection as in the recent simulations by Heggland et al. (2009), and by some mechanism transfer the same periodicity to the waves. In this work, we assume mainly that Alfvén waves are generated in the photosphere and have a white-noise spectrum, which would issue from the random buffeting motion by convection (or maybe photospheric magnetic reconnection). However, we also study the influence of the wave period in the resulting corona. Hence, we consider as well monochromatic wave drivers generating longitudinal modes with 10 s, 25 s, 50 s, 100 s, 150 s, 200 s, and 300 s periods (as one sinusoidal torsional wave creates two longitudinal waves, the periods of the Alfvén waves are twice the periods stated here). This analysis was started in Antolin et al. (2008), where it was shown that the most effective waves for coronal heating had periods between 100 s and 150 s. Here we extend the analysis by studying in detail the hydrodynamic response of the loop to the different wave periods. The more realistic random photospheric driver is considered for the rest of the parameter space study.

The standard model of the loop to which we apply the different parameters is the same as the one considered in Paper 1. That is, a 100 Mm length loop with an apex-to-base area expansion of 1000, a photospheric magnetic field of 2.3 kG and in which the Alfvén waves are generated by a random photospheric driver creating a white-noise frequency spectrum.

2.2. MHD Equations

The magnetic flux tube is modeled with the local curvilinear coordinates $(s, \phi, r)$ where $s$ measures the distance along the most external poloidal magnetic field line, $\phi$ is the azimuthal angle measured around the rotation axis of the flux tube, and $r$ is the radius of the tube. The structure of the loop is described by the following set of equations, where $z$ denotes the length along the central axis of the loop:

$$r = \int \cos \theta ds \quad (1)$$
$$z = \int \sin \theta ds, \quad (2)$$

where $\theta$ is the angle that the external magnetic field line makes with the radius of the loop (as a vector),

$$\theta = \theta_t + (\theta_r - \theta_t)f_n \quad (3)$$

$$\theta_r = -\arctan \left(\frac{-4H_0}{r}\right) \quad (4)$$

$$\theta_t = \arctan \left[ k \cosh \left(\frac{z - z_d}{H_0}\right) \right] \quad (5)$$

$$f_n = -\frac{1}{2} \left\{ \tanh \left[ \frac{z - z_d}{H_0} \right] - 1 \right\}. \quad (6)$$

In these set of equations, $k$ and $z_d$ are parameters describing the shape of the loop, namely, the rate of expansion at the footpoints (for instance, for an area expansion of 1000 we take $k = 3.48$ and $z_d = 6H_0$). $H_0$ corresponds to the scale height at the photosphere, $H_0 = 200$ km. $\theta_t$ in Equation (4) is a value that controls the area expansion near the photosphere. $\theta_t$ in Equation (5) controls the expansion of the loop at the apex. Equation (6) links smoothly these two parameters that describe different parts of the loop.

We take the 1.5D approximation:

$$\frac{\partial}{\partial \phi} = 0, \quad \frac{\partial}{\partial r} = 0, \quad v_r = 0, \quad B_r = 0, \quad (7)$$

where $v_r$ and $B_r$ are, respectively, the radial components of the velocity and magnetic field in the magnetic flux tube. In the considered approximation, conservation of magnetic flux defines the value of the poloidal magnetic field as a function of $r$ alone, $B_r = B_0(r_0^2/r)^2$, where $B_0$ is the value of the magnetic field at the photosphere and $r_0 = 200$ km is the initial radius of the loop. In the photosphere, the value of $\beta = 8 \pi p/(B^2_t + B^2_0)$
(the ratio of gas to magnetic pressures) is unity. We assume an inviscid perfectly conducting fully ionized plasma. The effects of thermal conduction and radiative cooling are considered.

The 1.5D MHD equations are written as follows. The mass conservation equation:

$$\frac{\partial \rho}{\partial t} + v_s \frac{\partial \rho}{\partial s} = -\rho B_s \frac{\partial}{\partial s} \left( \frac{v_s}{B_s} \right).$$  

The $s$-component of the momentum equation:

$$\frac{\partial v_s}{\partial t} + v_s \frac{\partial v_s}{\partial s} = -\frac{1}{\rho} \frac{\partial \rho}{\partial s} - g_s + \frac{v_s^2}{r} \frac{\partial r}{\partial s} - \frac{1}{4\pi \rho} B_\phi \frac{\partial}{\partial s} (rB_\phi).$$  

The $\phi$-component of the momentum equation:

$$\frac{\partial (r v_\phi)}{\partial t} + v_s \frac{\partial (r v_\phi)}{\partial s} = \frac{B_s}{4\pi \rho} \frac{\partial}{\partial s} (rB_\phi) + \mathcal{C}(t, s),$$  

the induction equation:

$$\frac{\partial}{\partial t} \left( \frac{B_\phi}{rB_s} \right) + \frac{\partial}{\partial s} \left( \frac{B_\phi}{rB_s} v_s - \frac{v_\phi}{r} \right) = 0,$$

and the energy equation:

$$\frac{\partial e}{\partial t} + v_s \frac{\partial e}{\partial s} = - (\gamma - 1) e B_s \frac{\partial}{\partial s} \left( \frac{v_s}{B_s} \right) - \frac{R - S}{\rho} + \frac{1}{\rho r^2} \frac{\partial}{\partial s} \left( r^2 \kappa \frac{\partial T}{\partial s} \right),$$

where

$$p = \frac{\rho k_B}{m} T, \quad e = \frac{1}{\gamma - 1} \frac{p}{\rho}. \tag{13}$$

In Equations (8)–(12) $\rho$, $p$, and $e$ are, respectively, density, pressure, and internal energy; $v_s$ is the poloidal component of the velocity along the external magnetic field line; $v_\phi$ is the toroidal (azimuthal) component of the velocity; $B_s$ and $B_\phi$ are, respectively, the poloidal and toroidal components of the magnetic field; $k_B$ is the Boltzmann constant; and $\gamma$ is the ratio of specific heats for a monatomic gas, taken to be 5/3. The $g_s$ is the effective gravity along the external poloidal magnetic field line and is given by

$$g_s = g_\odot \cos \left( \frac{z}{L} \pi \right) \frac{dz}{ds},$$

where $g_\odot = 2.74 \times 10^4$ cm s$^{-2}$ is the gravity at the base of the loop, $z$ is the length along the central axis of the loop, and $L$ is the total length of the loop. The $\mathcal{C}(t, s)$ in Equation (10) is a term which simulates the torque motions in the photosphere. It is responsible for the generation of Alfvén waves. For random photospheric perturbations generating a white-noise spectrum for the Alfvén waves, we have

$$\mathcal{C}(t, s) = 2r(s) [\text{rand1}(t) - 0.5] f \left\{ \tanh \left( \frac{s - 0.55 H_0}{0.055 H_0} \right) - 1 \right\} + \tanh \left( \frac{L - s - 0.55 H_0}{0.055 H_0} \right) - 1 \right\},$$

where $H_0$ denotes the pressure scale height at $z = 0$. We take $H_0 = 200$ km. The terms rand1$(t)$ and rand2$(t)$ are non-correlated functions that output a number randomly distributed between 0 and 1, which changes in time, and $f$ is a parameter that determines the strength of the torque. For the case of the photospheric driver generating monochromatic Alfvén waves, we have

$$R(T) = n_e n_p Q(T) = \frac{n^2}{4} Q(T),$$

where $n_e = n_e + n_p$ is the total particle number density ($n_e$ and $n_p$ are, respectively, the electron and proton number densities, and we assume $n_e = n_p = \rho/m$ to satisfy plasma neutrality, with $m$ being the proton mass) and $Q(T)$ is the radiative loss function for optically thin plasmas (Landini & Monsignori Fossi 1990), which is approximated with analytical functions of the form $Q(T) = \chi T^\gamma$. We take the same approximation as in Horii et al. (1997, please refer to their Table 1). For temperatures below $4 \times 10^4$ K, we assume that the plasma becomes optically thick. In this case, the radiative losses $R$ can be approximated by $R(\rho) = 4.9 \times 10^{10} \rho$ erg cm$^{-3}$ K$^{-1}$, after Sterling et al. (1993) (based on the empirical result of Anderson & Athay 1989), that the heating rate per gram over a large part of the chromosphere is roughly constant, at $4.9 \times 10^{10}$ erg g$^{-1}$ s$^{-1}$). In Equation (12), the heating term $S$ has a constant non-zero value which is non-negligible only when the atmosphere becomes optically thick. Its purpose is mainly for maintaining the initial temperature distribution of the loop.

### 2.3. Initial Conditions and Numerical Code

In the present model, a sub-photospheric region is considered by adding 2 Mm at each footprint of the loop, in which the radius of the loop is kept constant (hence keeping a constant magnetic flux). We take the origin $z = 0$ as the top end of this region. The loop is assumed to follow hydrostatic pressure balance in the sub-photospheric region and in the photosphere up to a height of $4H_0 = 800$ km, where $H_0$ is the pressure scale height at $z = 0$. The inclusion of the sub-photospheric region avoids unrealistic density oscillations due to the reflection of waves at the boundaries, thus avoiding any influence from the boundary conditions on the coronal dynamics. For the rest of the loop, density decreases as $\rho \propto h^{-4}$, where $h$ is the height from the base of the loop. This is based on the work by Shibata et al. (1989a, 1989b) in which the results of
2D MHD simulations of emerging flux by Parker instability exhibit such pressure distribution. The initial temperature all along the loop is set at $T = 10^4$ K. The density at the photosphere ($z = 0$) is set at $\rho_0 = 2.53 \times 10^{-7}$ g cm$^{-3}$, and, correspondingly, the photospheric pressure is $p_0 = 2.09 \times 10^5$ dyn cm$^{-2}$. As the plasma $\beta$ parameter is chosen to be unity in the photosphere, the equipartition magnetic field strength $B_{eq} = \sqrt{8\pi\rho_0}$ corresponds to $B_{eq} = 2.3$ kG. For loops having the later as the photospheric field strength, the corresponding value of the magnetic field at the top of the loop is then $B_{top} = 2.3$ G, 3.8 G, and 4.6 G, respectively, for loop expansions of 1000, 600, and 500.

In order to correctly resolve the dynamics in the chromosphere and transition region, we take a fine spatial resolution in the numerical scheme by setting the grid size $\Delta s = 0.025H_0 = 5$ km up to a height of $\sim 16,000$ km. Then, the grid size is allowed to increase as $\Delta s_{i+1} = 1.03\Delta s_i$ until it reaches a size of 20 km. The size is then kept constant up to the apex of the loop. We take rigid wall boundary conditions at the photosphere. The numerical schemes adopted are the CIP scheme (Yabe & Aoki 1991) and the MOC-CT scheme (Evans & Hawley 1988; Stone & Norman 1992). Refer to Kudoh et al. (1998) for details about the application of these schemes. We have chosen a rather long simulation time of 568 minutes (about 9.5 hr), in order to study the stability of the corona in the different models.

3. PARAMETRIC SPACE SURVEY

In Paper 1, it was shown that a corona heated by Alfvén waves is characterized by large dynamics. High-speed plasma flows, and large up and down shifts of the transition region due to the shocks are common features of this heating mechanism. In order to determine the average values of thermodynamic variables in the corona, the location of the two transition regions is tracked down in time. This is carried out for all the figures displaying coronal quantities in the present work.

3.1. Wave Dissipation

In the present model, the linearly polarized Alfvén waves have basically only one mechanism available in order to dissipate their energy, mode conversion. Due to the large density stratification of the atmosphere, Alfvén waves grow in amplitude and the problem easily becomes nonlinear. Alfvén waves can then convert a part of their energy to the longitudinal slow and fast modes during propagation. This conversion happens mainly while propagating from the photosphere to the chromosphere (passing from high-$\beta$ to low-$\beta$ plasmas), although important conversion processes also happen in the corona, as discussed below. The resulting longitudinal modes subsequently steep into shocks and heat the plasma. This mode conversion mechanism has been shown to be an efficient dissipation mechanism for Alfvén waves by which the corona can be heated for both open and closed magnetic field regions (Hollweg et al. 1982; Kudoh & Shibata 1999; Moriyasu et al. 2004; Antolin et al. 2008) and also for the generation of the fast and slow solar wind (Suzuki & Inutsuka 2006). Another dissipation mechanism, which may be playing an important role in our model, especially when considering the monochromatic wave driver in the photosphere, is through resonant damping. In this heating scenario, closed magnetic flux structures like loops serve as resonant cavities for Alfvén waves. For certain wave frequencies, the loop can resonate thus allowing a high transmission of these waves into the corona. This heating mechanism is further discussed in Section 3.3.1. For the mode conversion mechanism the density fluctuation is crucial for the efficient dissipation of the waves. As was shown in Paper 1 and other related works (see, for instance, Suzuki & Inutsuka 2006), the coronae emerging from Alfvén wave heating characterize by showing large density fluctuations. Mode conversion takes place wherever the sound and Alfvén speed have similar values (plasma $\beta \sim 1$ region), which is mainly the chromosphere, but mainly when the nonlinear effects are large. Nonlinear effects can be quantified by the ratio of azimuthal to longitudinal magnetic field (or velocities) $B_\phi/B_s$. As shown in Paper 1, this quantity takes values higher than 0.5 sporadically and ubiquitously in the corona due to the large density fluctuation caused by the longitudinal shocks. The large density fluctuation throughout the loop also causes the deformation of the Alfvén wave shape, which causes small-scale fluctuations of the magnetic pressure and leads to the generation of slow modes (Moore et al. 1991). Another factor playing an important role in the wave dissipation is the wave-to-wave interaction. In this closed magnetic field model, we have waves being generated at both footpoints and also reflection of waves at both transition regions. We thus have collision of waves and shocks at all times in the corona, which greatly enhances nonlinearity and shock strengths. This intermittent mode conversion in the corona leads to a bursty intensity profile similar to the usual X-ray intensity profiles of the solar corona (as those shown by Hinode/XRT, for instance). This has led Moriyasu et al. (2004) to propose the idea of nanoflares being the signatures of this nonlinear heating mechanism from Alfvén waves. It has also been shown from statistics of the resulting heating events that a power-law distribution of the intensities issues with an index steeper than 2 (cf. Paper 1), a scenario in which the bulk of the heating comes from the small nanoflare-like heating events (Hudson 1991).

3.2. General Characteristics

Figures 1 and 5–7 show the average in time of several quantities describing the thermodynamic state of the corona with respect to the photospheric rms azimuthal velocity field created by the torsional motions at the footpoints of the loop for each case of our parameter study. In panels (a) of Figures 1 and 5–7, we see the expected general tendency of the mean coronal temperature to increase with the amplitude of the photospheric velocity perturbation. This is expected since higher photospheric transversal velocities mean a higher energy flux into the loop (the converse is not always true as we will see below), as shown in panels (c) of Figures 1 and 5–7, which show the variation of the mean rms photospheric magnetic energy $(B^2_{\phi, ph}/8\pi)^{1/2}$ with the photospheric velocity amplitude. Higher energy fluxes from the waves generate stronger longitudinal shocks leading to a higher heating rate as long as conditions for mode conversion are met (see Section 3.1). This is shown in panels (e) corresponding to the same figures, where the volumetric heating rate $H$ is plotted (below we explain how we calculate this quantity). We see that conditions leading to long-term average temperatures

\[ H \]

The mean Alfvén speed in the corona obtained from heating by 100 s period waves in our model is $300$ km s$^{-1}$. This gives a wavelength on the order of one third of the loop size. Such long wavelengths and the large density fluctuations lead to the deformation of the wave shape and the subsequent generation of slow modes.
above 1 MK are not easily met. Only large expansions (above an area ratio of 600 between the photosphere and corona) together with long lengths (above 100 Mm) provide the necessary conditions. Also, the photospheric velocity amplitudes must be large enough. In the present case, coronae with average temperatures (over the entire simulation time) above 1 MK are obtained for $\langle v^2_{\phi,\text{ph}} \rangle^{1/2} > 1.6 \text{ km s}^{-1}$. On shorter timescales, temperatures in the corona can easily reach nanoflare-like temperatures above 1 MK, as shown in panels (g), which show the maximum temperatures that can be reached with Alfvén wave heating. Maximum temperatures show the same dependence with the photospheric velocity field as for the mean coronal temperature. Maximum temperatures between 2 MK and 5 MK are found for long-period waves (defined here as waves with periods above 100 s). This is further discussed in Section 3.3.1. As was found in Paper 1, the most efficient wave periods for the heating are between 100 s and 150 s. The 300 s waves also offer an interesting heating scenario. Their high power (as seen in panel (c) of Figure 1) combines with resonant damping to give the highest temperatures in the model. This case is discussed in detail in Section 3.3.1.

As the strengths of the shocks increase with the amplitude of the photospheric perturbations, the mass flux into the corona increases due to the higher magnetic pressure from the waves, thus increasing the density of the corona (panels (b)). The Alfvén speed consequently decreases on the one hand, while the sound speed increases on the other due to the higher temperatures, leading to a high increase of the plasma $\beta$ parameter (panels (c)), which is the ratio of gas to magnetic pressures $\beta = 8\pi p/(B^2_I + B^2_\phi)$. Due to the strong shocks permeating the corona, the plasma $\beta$ parameter takes values above 0.1 sporadically and ubiquitously in the corona, contributing to mode conversion processes. This behavior is also shared by the quantity $v_\phi/v_A$, which measures the nonlinear effects and therefore is the main contributor for mode conversion. This is crucial for the efficient dissipation of the waves in the corona, which therefore gets...
Nonlinear effects

Figure 2. Nonlinear effects quantified through the ratio of the azimuthal velocity to the Alfvén velocity, \(\langle|v_\phi|/v_A\rangle\). Here we plot the average value in time of this quantity along the loop for different models. Panel (a): base model, a loop of length 100 Mm, photospheric magnetic field of 2.3 kG, and area expansion of 1000 between photosphere and corona. Panels (b)–(d): same as the base model but with a photospheric magnetic field of 1 kG, with an area expansion of 500, with a length of 60 Mm, respectively. For each model, three cases with different photospheric rms azimuthal velocity fields are plotted, the values of which are written in the upper right corner of each panel. The dotted lines correspond to a low value of \(\langle v_\phi^2 \rangle^{1/2}\) (leading to low coronal temperatures). The solid line corresponds to the value of \(\langle v_\phi^2 \rangle^{1/2}\) for which the highest temperatures are found. The dashed line corresponds to a value for which the corona collapses during the simulation (see Section 3.2.1).

uniformly heated, as discussed in Section 3.1. The average value in time of this quantity along the loop is plotted in Figure 2. Panel (a) corresponds to our base model: a loop of length 100 Mm, a photospheric magnetic field of 2.3 kG, and an area expansion of 1000 between the photosphere and the corona, in which a white-noise spectrum of Alfvén waves is generated at the footpoints. Panels (b)–(d) correspond to variations of the base model: with a photospheric magnetic field of 1 kG (panel (b)), an area expansion of 500 (panel (c)), and a length of 60 Mm (panel (d)). For each model, different values of the rms photospheric velocity field are plotted. The solid line corresponds to the value of \(\langle v_\phi^2 \rangle^{1/2}\) for which the highest temperatures are obtained in each model. As a general rule, in all our models a high value of the ratio \(v_\phi/v_A\) in the corona \((\gtrsim 0.3)\), or correspondingly in the photosphere \((\gtrsim 0.06)\), is necessary in order to obtain a million degree corona. For higher amplitudes of the rms photospheric velocity field (dashed lines), the nonlinear effects are reduced (except for the case of the short loop with 60 Mm, which we will discuss in more detail in Section 3.3.4) and the loop enters a regime in which the corona cannot be maintained over long periods of time. This regime is discussed in Section 3.2.1.

The uniform heating of the corona can be quantified by comparing the obtained temperatures with the predicted coronal temperatures based on the Rosner–Tucker–Vaina (RTV) scaling law (Rosner et al. 1978). This is demonstrated in Figure 3. Panels (a)–(d) display the mean temperature in the corona with respect to the predicted temperature from the RTV scaling law, and correspond, respectively, to the photospheric driver study, the photospheric magnetic field, the loop expansion study, and the loop length study. It can be noted that in general the RTV scaling law fits remarkably well with the obtained coronal temperatures.

7 The photosphere is pointed out in the figure by the location close to the footpoints where \(|v_\phi|/v_A\) acquires its minimum value. In the sub-photospheric region, the ratio increases again due to the low Alfvén velocity.
valuated, mainly for short-period waves (<100 s, as discussed in
Section 3.3.1) and low photospheric velocity amplitudes. The
error increase with photospheric velocity amplitude is due to the
stronger shocks which input large amounts of chromospheric
material in the corona (creating high spicule-like events) and
therefore disrupts the local energy balance. Since the RTV
scaling law is found to be well satisfied, we estimate from it
the volumetric heating rate $H$. As shown in Rosner et al. (1978),
we have

$$H = 9.8 \times 10^4 \rho^{7/6} L^{-5/6}, \quad (18)$$

in erg s$^{-1}$ cm$^{-3}$. The estimations resulting from this equation
are plotted in panels (e) of Figures 1 and 5–7.

Despite the higher momentum of the waves as the amplitudes
of the photospheric driver increase, the upward shifts of the
transition region (spicule-like events) remain roughly constant.
This has been previously found by Hollweg et al. (1982). As
explained in that paper for the case of open flux tubes, given a
high-amplitude shock we will have a faster upward rise of the
transition region and thus also a longer duration for the following
shock to reach the transition region, hence giving the latter more
time to recede from gravity to lower heights. In the present case
of closed flux tubes, we have found the same behavior, thus
producing a mean length of the corona that is roughly constant
as seen in panels (f) of Figures 1 and 5–7. However, when the
photospheric velocity amplitude exceeds a critical value this is
no longer the case. Indeed, a sharp decrease of the coronal length
can be noted when the photospheric azimuthal velocities exceed
a certain critical value which depends mostly on the geometrical
parameters of the loop (length and expansion). The critical
photospheric velocity decreases the longer the periods of the
waves as discussed in Section 3.3.1. For photospheric velocities
higher than the critical velocity, the corona enters an unstable
regime in which the temperature, density (and consequently the
plasma $\beta$ parameter) stop increasing. These cases are marked
with blank symbols in all panels. We will now discuss this
corona collapse regime.

3.2.1. Corona Collapse

In order to create a corona, the wave heating coming from
mode conversion of Alfvén waves (cf. Section 3.1) has to exceed
the losses due to radiation and (downward) conduction. The
rapidity with which this energy balance is reached and a corona
forms will depend on many parameters, such as the initial
conditions as well as geometrical aspects (length and expansion
of the loop, for instance). In panels (h) of Figures 1 and 5–7,
we show the time span of the corona over the entire simulation time
(568 minutes). We can see that for each set of the considered loop
parameters there is a range of photospheric velocity amplitudes
for which the energy balance in the corona is maintained over
most of the simulation, i.e., for which the corona is stable.
The time span of the corona in this region is roughly constant.
However, there is a critical velocity above which the stability of
the corona is compromised and the time span drops off sharply.
These cases are marked with blank symbols in all panels. For
these cases the corona can break down at some point and reform
at a later moment, or not be reformed at all. More specifically, we
have defined a stable corona as a corona that lasts for more than
60% of the total simulation time, which corresponds roughly
to 5.7 hr. The value of the photospheric magnetic field (and
hence the value of the background magnetic field) does not
seem to influence the critical photospheric velocity at which
the instability sets in, as seen in panel (h) of Figure 5. For

all the values considered for the photospheric magnetic field,
the corona gets unstable for $(\psi_0^2 / \phi_0^2)^{1/2} \gtrsim 2.2$ km s$^{-1}$ (see
Section 3.3.2). Loops with thinner areas of cross sections and
shorter lengths have much smaller stable regimes (see Sections
3.3.3 and 3.3.4). Unstable coronae are seen to happen only for
wave periods above 100 s. The critical velocity amplitude above
which instability sets in is also dependent on the wave period.
The longer the period the lower the critical velocity. For instance,
for 100 s and 200 s waves we find unstable coronae already at
2.8 km s$^{-1}$ and 1.8 km s$^{-1}$, respectively.

The unstable regime can be understood partly by analyzing the
behavior of the volumetric heating rate. As shown in panels
(e) of Figures 1 and 5–7, this quantity reaches a maximum for
values of the photospheric velocity field which are generally
lower than the critical velocity for which the corona collapses.
The volumetric heating rate is then either constant or slightly
decreases. Correspondingly, the mean temperature and density
in the loop reach maximum values after which they are either
constant or decreasing. The presence of these maxima can be
understood by means of the energy balance in the loop, which
may be approximated in the following way:

$$H = \frac{n^2}{4} Q(T) + \kappa_0 T_7^{7/2} \frac{L^2}{L^2}, \quad (19)$$

where the first term on the right corresponds to the radiative
losses, and the second term corresponds to thermal conduction.
For values of the photospheric velocity field lower than the
critical value we have a constant volumetric heating rate $H_{\text{max}}$
temperatures corresponding to an optically thin cooling which
can be approximated by $Q(T) = \chi T_7^{7/2}$ with $\chi \sim 10^{-18} K$ (we take the same approximation for temperatures above $10^5 K$ as in
Rosner et al. 1978) and a roughly constant length of the corona $L$.
The maximum value of the volumetric heating rate then naturally
sets a maximum value for the density and temperature. We have

$$n = \left[ \frac{4}{\chi} T^{-1/2} \left( H_{\text{max}} - \kappa_0 T_7^{7/2} \right) \right]^{1/2}. \quad (20)$$

This equation defines a maximum density value $n_{\text{max}} =
\frac{1}{2} H_{\text{max}} T_{\text{max}}^{1/2}$ for a temperature $T_{\text{max}} = \left( \frac{H_{\text{max}} L}{\kappa_0} \right)^{2/7}$.
Replacing by numerical values $H_{\text{max}} \sim 3 \times 10^{-3}$ erg s$^{-1}$ cm$^{-3}$,
$L \sim 8 \times 10^9$ cm, and $\kappa_0 \sim 10^{-6}$ erg s$^{-1}$ K$^{-1}$ cm$^{-3}$, we obtain a
maximum density of $n_{\text{max}} \sim 5 \times 10^9$ cm$^{-3}$ for a temperature of
$T_{\text{max}} \sim 6 \times 10^5 K$, which roughly matches the critical temperature
and density values we obtain.

Figure 2 shows that nonlinear effects are reduced in the
unstable regime. Hence, mode conversion is reduced leading to
a saturation of the volumetric heating rate. The saturation is
due to the height of the spicules. As explained in the previous
section, the height of the transition region is roughly unaffected
by the amplitude of the photospheric driver, as long as
this one does not exceed the critical value. When the critical
amplitude is exceeded, spicules become much longer due to the
decreasing effective gravity along the loop. The cooling effect
on the corona is therefore large, and the volumetric heating rate
from the waves is saturated. Correspondingly, for values of the
photospheric velocity close to the critical velocity the energy
balance along the loop is not well maintained, and the error
from the RTV scaling law increases, as seen in Figure 3. This
results in the collapse of the corona. As stated previously, long-
period waves have shorter critical velocity than short-period
waves. This is due to the stronger and less frequent shocks

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obtained with longer periods as discussed in Section 3.3.1. For 300 s waves, the obtained coronae are unstable even with low-amplitude photospheric velocities (except for only one case). Long-period waves can carry large amounts of chromospheric material into the corona, increasing their density as shown in panel (b) of Figure 1. Since the energy flux into the corona is constant in time, the heating per unit mass decreases in time, an effect which is stronger for long periods due to the lower number of shocks in the corona at a given time.

For a small number of cases with low amplitudes of the long-period waves (cases for which the cooling effect from the spicules is not important) the coronae reach a critical state in which they are susceptible to a thermal instability, by which the corona rapidly cools down (in the order of minutes) and the loop is evacuated. A similar cooling event is obtained for loops that are heated toward their footpoints (Antiochos et al. 1999; Müller et al. 2003; Mendoza-Briceño et al. 2005), a phenomenon termed “catastrophic cooling,” which has been proposed as the physical explanation for coronal rain. The cyclic pattern of heating and cooling in the loops (“limit cycles,” as termed by Müller et al. 2003) is only seen for some cases with low amplitudes of the monochromatic driver generating long-period waves. In all other cases, for instance, for thinner and shorter loops or for high amplitudes of the random photospheric driver, the collapse of the corona that is obtained is of a different nature than that of catastrophic cooling. In these cases, the density of the corona (and consequently the radiative losses) does not gradually increase, as occurs in the case of footpoint heating leading to catastrophic cooling. Instead, the long spicules shorten dramatically the length of the corona, disrupting the local energy balance, and no cool condensation is formed. In the cases with low-amplitude long-period waves in which we obtain a cyclic collapse of the corona, no local cool condensations are obtained. Furthermore, this cooling down phenomenon is obtained in rather isolated cases in which the waves issuing from both footpoints remain in phase during the entire simulation. On the other hand coronal rain has been observed to be a rather common phenomenon of active regions. We thus conclude that these cases do not correspond to the observed coronal rain. Whether Alfvén waves can reproduce coronal rain, as catastrophic cooling does, despite the uniform heating they produce, is an interesting matter which we have investigated in detail in Antolin & Shibata (2009). It found that when Alfvén waves are a non-negligible source of energy in coronal loops, catastrophic cooling is inhibited due to the characteristic uniform heating. We will now discuss individual features of each set of parameters.

### 3.3. Individual Characteristics

#### 3.3.1. Photospheric Driver

The loop model in this section consists of a 100 Mm length loop with an expansion factor of 1000 and a photospheric magnetic field of 2.3 kG, and in which monochromatic Alfvén waves are generated at both footpoints.

Panels (a)–(h) of Figure 1 display the characteristics of the coronae produced by monochromatic slow and fast MHD waves resulting from the mode conversion of Alfvén waves. We can see that short-period (\(\leq 50\) s) and long-period (\(\geq 100\) s) waves produce very different coronae. Long-period waves produce hotter and denser coronae than short-period waves as shown in panels (a) and (b). Coronae produced by long-period waves are subject however to the unstable regime discussed in Section 3.2.1 when the photospheric velocity amplitudes are high, as can be seen in panel (h), and by the blank symbols in all the panels. For wave periods below 150 s, for the same velocity amplitude we obtain the higher the coronal temperatures the longer the period, and we find temperatures above 1 MK for velocities \((v^2_\phi)^{1/2}\) in the range 0.9–1.6 km s\(^{-1}\) for 100 s and 150 s period waves. Waves with lower periods (high frequency) are rapidly damped when propagating through the lower atmospheric layers. On the other hand, since longer periods imply longer wavelengths, the number of shocks heating the corona at a given time is reduced and the corona is less uniformly heated. This is shown in panel (a) of Figure 3, where the match with the RTV scaling law is plotted (Rosner et al. 1978).

Musielak et al. (2007) have shown that torsional Alfvén waves have cutoff-free propagation for the case of thin magnetic flux tubes, and thus can carry large amounts of energy into the corona. Verth et al. (2009, 2010) have pointed out however that the assertion made by Musielak et al. (2007) is valid only when the temperature in the flux tube does not differ from that of the external plasma. In the present case, the flux tube is isolated but presents velocity gradients (which issue from the density stratification and expansion of the magnetic flux tube), also a case in which a period cutoff would be theoretically introduced. Routh et al. (2007) have considered this problem analytically and shown that the period cutoff for torsional Alfvén waves is local (as opposed to global, where coupling to gravity or density stratification exists), introduced by gradients of the characteristic wave velocities. Caution should be taken, however, when applying their results, since it contains an approximation which may not be valid for thick flux tubes, as pointed out by Verth et al. (2010). However, their main result concerning the existence of the period cutoff for thick flux tubes remains valid, as shown by the previous paper. Due to the high nonlinearity with which the Alfvén waves operate in the present model, it is hard to estimate the influence from the period cutoff, through which long-period waves would suffer and their efficiency for heating the solar corona would be reduced. Since we have a very dynamic transition region in the present model even in the presence of a short-period cutoff, long-period waves are able to propagate into the corona. This is also the case for Matsumoto & Shibata (2010). In the later, basically the same numerical model is used, with the difference that an open flux tube is modeled. No influence of a cutoff has been reported. A proper study of the influence of the period cutoff would take us too far from the purpose of this paper; please refer to Verth et al. (2009, 2010) for further discussion on this subject.

Apart from the cutoff period for Alfvén waves the normal cutoff period for longitudinal waves is also present. In our model, the value of this period cutoff is close to 200 s. Hence, a large fraction of longitudinal waves with periods larger than 200 s issuing from mode conversion occurring below the transition region would not be able to propagate into the corona. This may explain the low heating efficiency from the 200 s period waves. For the 300 s waves however, we still can have a hot corona as seen in panel (a). We will discuss why this is so further ahead.

Long-period waves can create very hot heating events close to 5 MK as shown in panel (g), accounting for the observed nanoflares with instruments such as Hinode/XRT (Golub et al. 2007). Despite the fact that short-period waves do not contribute substantially to the hot temperatures of the corona, they do have an important effect for the thermal stability of the loop. As
Figure 4. Map of the power spectrum in logarithmic scale of the longitudinal velocity component $v_s$ (left) and the azimuthal velocity component $v_\phi$ (right) for the first 20 Mm along a loop where 300 s monochromatic longitudinal waves are generated (from mode conversion of 600 s Alfvén waves).

(A color version of this figure is available in the online journal.)

previously stated, the coronae obtained with short-period waves are more uniform due to the higher number of shocks permeating the corona. The large cool mass upflows into the corona due to the waves are reduced, resulting in longer lengths and time spans of the corona (panels (f) and (h)).

In order to better understand these results, we plot in panel (c) of Figure 1 the mean azimuthal magnetic energy $B_\phi^2/8\pi$ at the photosphere with respect to the photospheric velocity amplitude for each period. $B_\phi$ is a measure of the twist exerted at the footpoints of the loop, which increases with the period of the wave. Indeed, we can see that for the same input of magnetic energy, there is a shift toward lower amplitudes of the photospheric velocity field the longer the period of the wave. Hence, it is to be expected that longer period waves produce hotter coronae as shown in panel (a).

The large difference that can be seen in the photospheric azimuthal magnetic energy (panel (c)), and in general in all panels of Figure 1 between the 300 s waves case and the other periods, points to the presence of an additional heating mechanism. Indeed, apart from mode conversion there is another heating mechanism which seems to be playing an important role, especially when considering a monochromatic wave driver. Closed magnetic structures such as loops may act as resonant cavities for the Alfvén waves, which can suffer from reflection due to the steep gradients of the Alfvén velocity and be trapped in the corona. Resonances can increase the transmission coefficient from the waves, thus allowing large energy fluxes into the corona.

In Figure 4, we plot the map of the power spectrum at each point along the first 20 Mm of a loop with 300 s monochromatic waves for the longitudinal velocity component $v_s$ corresponding to the longitudinal modes, and azimuthal velocity component $v_\phi$ corresponding to the Alfvén waves. In this case, the rms photospheric velocity amplitude is $\langle v_\phi^2 \rangle^{1/2} \sim 0.75$ km s$^{-1}$, and we can see a clear resonance pattern from the corona down to the chromosphere. In the longitudinal velocity map, the fundamental mode at 300 s and the first (150 s), second (100 s), and third (75 s) harmonics coming from the mode conversion of the Alfvén waves can be clearly seen. However, in the azimuthal velocity map, the fundamental mode at 600 s and only the even harmonics (second, fourth, and so on) can be seen. Since we have set the monochromatic driver to generate waves that are in phase, the absence of the odd harmonics is simply due to a destructive interference between the Alfvén waves generated at both footpoints. Nevertheless, since mode conversion can happen in a timescale of minutes, before the disappearance of the odd harmonics mode conversion from these waves occurs resulting in the odd harmonics of the longitudinal velocity map.

Hollweg (1984) was the first to consider resonant damping in the case of a loop, where the later is approximated by a three-layer model in which the Alfvén velocity increases exponentially in the boundary layers (chromosphere and transition region) and is constant in the corona. Hollweg (1984) showed that when a wave is generated at one footpoint, the transmission coefficient into the corona can be written as

$$T \approx \left(1 + \left(\frac{v_\phi \sin(kL_c)}{2\pi h\omega}\right)^2\right)^{-1},$$

(21)
where $v_{A,c}$ is the Alfvén speed in the corona, $L_c$ is the length of the corona, $h$ is the pressure scale height, $\omega$ is the frequency of the wave, and $k = \omega/v_{A,c}$ is the wavenumber. The coronal resonances are excited for the periods:

$$\tau_{\text{res}} = \frac{2L_c}{mv_{A,c}},$$  

where $m = 1, 2, 3, \ldots$. At these periods the transmission coefficient has its maximum value. Equation (22) is simply the travel time for the Alfvén waves back and forth between the boundaries of the resonant cavity, and hence denotes the normal oscillating modes for the Alfvén waves. In that work, the height of the transition region was however not considered, which is important in our model. Indeed, we have seen that the height of the spicules can be large. Furthermore, we also consider a sub-photospheric region at both footpoints. We can estimate the resonant periods in our model by adding the travel time of the waves in the regions below the transition regions. A more precise estimation of the resonant periods would take us too far from our present parameter study, and thus is left as future work.

We have

$$\tau_{\text{res}} = \frac{2L_{fp}}{mv_{A,fp}} + \frac{2L_c}{mv_{A,c}},$$  

where $L_{fp}$ is the length of the region below the transition region and $v_{A,fp}$ is the mean Alfvén velocity in that region (all quantities denote averages over time). Inserting mean values of the 300 s waves case where resonance is detected: $L_c = 84$ Mm, $L_{fp} = 10$ Mm, $v_{A,c} = 440$ km s$^{-1}$, and $v_{A,fp} = 190$ km s$^{-1}$, we obtain $P \sim 590/m$ s, which matches well the resonant periods of the Alfvén waves (and hence the resulting periods for the longitudinal waves).

3.3.2. Photospheric Magnetic Field

In Figure 5, we plot the results of the parameter survey for different values of the photospheric magnetic field $B_{s,0}$. We test $B_{s,0} = 2.3$ kG, 1.5 kG, and 1 kG. Here the model consists of a 100 Mm length loop with an expansion factor of 1000 and a random photospheric driver. Having set in our model the value of the photospheric pressure to $p_0 = 2.09 \times 10^5$ dyn cm$^{-2}$, the equipartition magnetic field strength $B_{eq} = \sqrt{8\pi p_0}$ corresponds

Figure 5. Results of Alfvén wave heating with different photospheric magnetic fields. Fields of 2.3 kG (circles), 1.5 kG (triangles), and 1 kG (squares) are tested. See the legend of Figure 1 for explanation of the panels.
to $B_{p,0} = 2.3$ kG. In this case, we use the more realistic random photospheric driver for the generation of Alfvén waves. From the panels of Figure 5 we can see that the thermodynamical properties of the corona do not change considerably with the value of the photospheric magnetic field. For low amplitudes of the photospheric velocity field ($\langle v_{\phi}^2 \rangle^{1/2} \lesssim 1.1$ km s$^{-1}$), the photospheric magnetic energies, temperatures, densities, lengths, and time spans of the corona are similar as shown in panels (a)–(c) and (f)–(h). Also, the critical velocity above which the corona is unstable is roughly the same: $\langle v_{\phi}^2 \rangle^{1/2} \sim 2.2$ km s$^{-1}$. Panels (a) and (b) of Figure 2 show that the nonlinear effects are also roughly similar, since these are rather independent on the background magnetic field. For photospheric velocities between $1.2$ km s$^{-1}$ and $2.2$ km s$^{-1}$, however, hotter and denser coronae are obtained for a stronger photospheric magnetic field, as shown in panels (a) and (b) of Figure 5. For instance, for a photospheric velocity amplitude of $\sim 2$ km s$^{-1}$ the coronal temperature and density are, respectively, $7.4 \times 10^{5}$ K and $2.5 \times 10^{8}$ cm$^{-3}$ for $B_{p,0} = 1$ kG, and $1.1 \times 10^{6}$ K and $5.5 \times 10^{7}$ cm$^{-3}$ for $B_{p,0} = 2.3$ kG. However, the plasma $\beta$ parameter is roughly equal for velocities $\langle v_{\phi}^2 \rangle^{1/2} > 2$ km s$^{-1}$ as seen in panel (d). For lower values of the photospheric velocity field we obtain higher plasma $\beta$ the lower the value of the photospheric magnetic field.

The disparities between the three cases can be understood by the different pressure distributions along the loop obtained by varying the photospheric magnetic field. Since the equipartition magnetic field corresponds to the case $B_{p,0} = 2.3$ kG, the other cases have higher plasma $\beta$ at the same height in the photosphere and the chromosphere. As the amplitude of the torsional motions in the photosphere increases, the magnetic pressure increases and pushes photospheric and chromospheric matter upward. Since the magnetic pressure depends not only on the square of the torsional motions but also on the square of the longitudinal magnetic field, the uplift effect is stronger for the stronger photospheric magnetic field. Then, the gas pressure $p$ increases faster the higher the magnetic field. A higher coronal gas pressure implies a higher volumetric heating rate as shown by Equation (18), and illustrated in panel (e) of Figure 5, thus explaining the higher temperatures.

New observations with the Solar Optical Telescope on board the Hinode satellite have shown patches of strong magnetic of 1–1.5 kG scattered uniformly all over the surface of the Sun, especially in quiet-Sun and polar regions (Tsuneta et al. 2008). Our results indicate that Alfvén waves that may be generated at the footpoints of loops spanning from these regions do not have energy limitations as far as the photospheric magnetic field is concerned.

3.3.3. Loop Expansion

We now consider different expansions of the loop displaying area ratios of 1000, 600, and 500 between the corona and the photosphere. The loop is 100 Mm in length and has a photospheric magnetic field of 2.3 kG. The Alfvén waves are generated with the random photospheric driver.

Figure 6 displays the influence of the expansion of the loop in the thermodynamic properties of the corona. As the expansion of the loop is reduced, the temperature and density in the corona are reduced as well, as shown in panels (a) and (b), despite the same photospheric magnetic energy at the footpoints (panel (c)). For the loop with an expansion factor of 500 all the average temperatures in the corona are well below 1 MK (in this case, the maximum achieved average temperature for a stable corona is $7.4 \times 10^{5}$ K, which appears to be an exception due to the large difference with the other cases). Consequently, the plasma $\beta$ differs roughly by 1 order of magnitude in the corona between the loops with expansion factor 1000 and 500 (panel (d)). Together with the temperatures and densities of the corona, the critical velocities above which we have unstable coronae are reduced as well with lower loop expansions, as shown in panel (b). While the critical velocity above which the corona collapses is $\langle v_{\phi}^2 \rangle^{1/2} \sim 2.2$ km s$^{-1}$ for a loop expansion of 1000, the corresponding critical velocities for loop expansions of 600 and 500 are $\sim 1.7$ km s$^{-1}$ and $\sim 1.3$ km s$^{-1}$, respectively. In the stable velocity range, the lengths of the coronae are comparable, although there are two cases for the expansion factor of 500 for which the corona is barely stable and the loop lengths are reduced by half, namely, $\langle v_{\phi}^2 \rangle^{1/2} \sim 0.9$ and $\sim 1$ km s$^{-1}$. We have also performed simulations with loop expansions of 300 but no stable corona was found.

As discussed in Section 2.1, the expansion of magnetic flux tubes is a parameter that can greatly constrain the wave heating. Thin flux tubes allow large energy flows from Alfvén waves into the corona since they do not introduce any Alfvén velocity gradients (as long as the external temperature and internal temperature of the flux tubes do not differ), thus allowing cutoff-free propagation of Alfvén waves (Musielak et al. 2007; Verth et al. 2009). When expansion is strong enough to introduce velocity gradients, the spectrum of Alfvén waves that do not become evanescent is reduced (Routh et al. 2007), as discussed in Section 3.3.1 (caution should be taken however when applying the results stated in the later paper, as pointed out by Verth et al. 2009). However, in our case we have lack of heating for thinner flux tubes, while the strong expansion case of 1000 can easily achieve temperatures above 1 MK.

A simple calculation can illustrate the dependence of mode conversion on the expansion of the loop. Assuming a typical Alfvén speed of 10 km s$^{-1}$ in the upper photosphere/ lower chromosphere and a period of 100 s, we obtain a wavelength of 1000 km for Alfvén waves propagating from the photosphere. Now, all the loops considered here display roughly the same initial expansion in the photosphere. We have an expansion of roughly 1000 km in the first 1000 km above the photosphere, thus matching the wavelength of the Alfvén wave. A slightly higher expansion has been reported by Jess et al. (2009) by comparing the H$\alpha$ continuum with H$\alpha$ core images in observations of a bright point with the SOUP instrument of SST. Since this region is the region where the plasma $\beta$ is close to unity, we have ideal conditions for mode conversion for the Alfvén waves. For instance, deformation of the wave shape and excitation of slow modes should take place (Moore et al. 1991). Since our three cases have roughly the same initial expansion, this implies that mode conversion taking place higher up in the chromosphere is very important for the Alfvén wave heating to be effective.

The most important influence on the heating from the expansion of loops in our case has to do with the nonlinear effects. Higher expansions produce higher azimuthal velocities in the corona, which influence flows along the loop through the centrifugal force (cf. the third term on the right-hand side of Equation (9)). This in turn increases the density in the corona as seen in panel (b) of Figure 6, thus decreasing the Alfvén velocity. Consequently, the ratio $v_{\phi}/v_A$, which measures the nonlinear effects, increases. This is illustrated in panels (a) and (c) of Figure 2, where this ratio is plotted for loop expansions of 1000 and 500, for different amplitudes of the photospheric
velocity field. From basic concepts it can be easily shown that
\[
\frac{v_\phi}{v_A} \propto A_{\rho}^{1/4},
\]
where \(A\) is the area expansion coefficient. As seen in Paper 1, \(v_\phi/v_s\) becomes high ubiquitously and sporadically in the corona. When this happens, nonlinear effects are large and energy is transferred from the Alfvén mode to the longitudinal slow and fast modes, which steepen into shocks and heat the plasma (see Section 3.1). Hence, the reason for the absence of heating in our thin loops is not the lack of energy flux or larger radiative losses but a lack of dissipation of the waves.

3.3.4. Loop Length

Observations of coronal loops and posterior analytical studies based on the energy balance in these closed magnetic field structures have shown that the coronal temperature in uniformly heated loops increases with the length of the corona (Rosner et al. 1978; Serio et al. 1981). In order to study the effect of length on Alfvén wave heating here, we consider coronal loops with lengths of 100 Mm, 80 Mm, and 60 Mm. The loops have the same expansion factor, namely 1000, and a photospheric magnetic field of 2.3 kG. The waves are generated with the random photospheric driver.

Figure 7 shows the effect of loop length in the creation of the corona from Alfvén wave heating. The results in this case are similar to the previous case in which the expansion of the loop is considered. We can see that as the length of the loop is reduced, the heating of the loop is dramatically reduced (panel (a)), despite the similar magnetic energy input at the footpoints (panel (c)). Already for the 80 Mm length loop we cannot obtain a corona with an average temperature above 1 MK. Densities are also reduced and therefore also the plasma \(\beta\) (panels (b) and (d)). The sensitivity of the coronae to the loop length can also be seen in panels (f) and (h), where we can see that the range of photospheric velocities over which the coronae can be created and maintained is considerably reduced with respect to all the previous cases. The critical velocities above...
which the coronae collapse are $\langle v_\phi^2 \rangle^{1/2} \sim 1.1$ and $\sim 0.6$ km s$^{-1}$, respectively, for 80 Mm and 60 Mm lengths. For photospheric velocity ranges in which the corona is stable, we can see from panel (f) that the lengths of the corona vary considerably. For $L = 80$ Mm, the lengths vary between 25 Mm and 50 Mm. For $L = 60$ Mm, we have only two stable cases with lengths between 10 Mm and 20 Mm.

The lack of wave heating can be understood partly by considering the number of shocks at any time heating the corona. In Section 3.3.1, we showed that long-period waves produce hot coronae while short-period waves account for their stability by heating them uniformly. The most efficient period range for the heating was found to be between 100 s and 150 s for the longitudinal waves, thus 200 s and 300 s for the Alfvén waves. For a photospheric velocity of $\sim 1$ km s$^{-1}$, typical Alfvén velocities in the corona are $\sim 400$ km s$^{-1}$ and $\sim 300$ km s$^{-1}$ for loop lengths of 80 Mm and 60 Mm, respectively (as derived from panel (b)). Taking a period of 200 s, this gives wavelengths of 80 Mm and 60 Mm for the Alfvén waves, respectively, which is just the length of the loops. We see that the wave has barely the distance to propagate one wavelength before reaching the other footpoint, where the dense sub-photospheric regions will not allow an easy reflection. Taking a roughly constant sound speed in the corona, it is easy to see that the necessary distance for shock formation will be at least on the order of a wavelength (in the case of a high-velocity amplitude). Since both footpoints generate Alfvén waves, we then may have a maximum of four shocks propagating in the corona at any time (neglecting all other dissipative mechanisms such as the wave-to-wave interaction), and may not easily reflect in the transition regions due to their long wavelengths. The same reasoning applied to a 100 Mm length loop gives roughly 12 shocks propagating at any time. Furthermore, in the later case shocks can easily reflect at the transition region and get trapped in the corona, thus increasing the dissipation in the corona.

Figure 2 shows that nonlinear effects are considerably reduced for shorter loop lengths. The highest value of the ratio $v_\phi/v_A$ for stable coronae is about 0.1, which is not enough for mode conversion to be efficient. The main reason for the lack of hot
corona in short loops is the same reason for their instability. Due to the shorter length, the effective gravity is significantly reduced and the height of the spicules increases considerably as shown in panel (f) of Figure 7. As the amplitudes of the waves increase, large amounts of cool matter are input into the loop. Spicules have then a stronger cooling effect the shorter the loop length.

4. DISCUSSION AND CONCLUSIONS

Alfvén waves constitute one of the main candidates for heating the solar corona. Theoretically easy to be generated from convective turbulent motions in the photosphere, it has been shown that these waves are able to carry sufficient amounts of energy in order to balance energy losses from radiation and conduction, and heat the corona up to the observed few million degrees (Uchida & Kaburaki 1974; Wentzel 1974; Hollweg et al. 1982; Poedts et al. 1989; Ruderman et al. 1997; Kudoh & Shibata 1999). Finding a suitable dissipation mechanism is a very difficult task, which has spawned a large active research community in solar physics. In this work, we have considered a model in which mode conversion acts as the dissipative mechanism. More precisely, through nonlinear effects based on density fluctuations and wave-to-wave interaction in the chromosphere and corona, the Alfvén mode is able to transfer some part of its energy to the fast and slow modes, which steepen into shocks and heat the plasma.

We have conducted a parameter survey in which the effect of geometrical quantities such as the loop expansion and the loop’s length on the efficiency of Alfvén wave heating is studied. We further investigate the effect on the heating of other physical parameters such as the photospheric magnetic field and the generation of Alfvén waves with a monochromatic and white-noise spectrum in the photosphere.

In Figure 8, we plot the volumetric heating rate with respect to the considered parameters of the loop: period of the monochromatic longitudinal waves issuing from mode conversion of Alfvén waves (top left panel), photospheric magnetic field (top right panel), expansion of the loop (bottom left panel), and loop length (bottom right panel). The volumetric heating rate for each case corresponds to its extremum values in the range between $\langle \psi_\phi^2 \rangle^{1/2} \sim 1.3$ and $2.3 \text{ km s}^{-1}$ found in panels (e) of Figures 1 and 5–7.

Figure 8. Volumetric heating rate with respect to the considered parameters of the loop: period of the monochromatic longitudinal waves issuing from mode conversion of Alfvén waves (top left panel), photospheric magnetic field (top right panel), expansion of the loop (bottom left panel), and loop length (bottom right panel). The volumetric heating rate for each case corresponds to its extremum values in the range between $\langle \psi_\phi^2 \rangle^{1/2} \sim 1.3$ and $2.3 \text{ km s}^{-1}$ found in panels (e) of Figures 1 and 5–7.
height comparable to the wavelength of the Alfvén wave, which leads to the deformation of the Alfvén wave and excitation of slow modes (Moore et al. 1991). Since the plasma $\beta$ parameter in that region is close to unity, further mode conversion is expected. Alfvén waves have long wavelengths and in order for them to convert into longitudinal waves which steep into shocks they need to propagate relatively long distances. Loops with lengths lower than 80 Mm cannot be heated by Alfvén waves in the present model. Caution must be taken however when drawing conclusions from these results. When calculating the lengths of loops in observations what is actually calculated is the length of the corona, which is the visible part of loops in EUV or X-ray images. In our model, the lengths of the coronae with average temperatures of $\sim 1$ MK we obtain with Alfvén wave heating oscillate between 50 Mm and 80 Mm with a mean around 70 Mm. Furthermore, we have defined a stable corona, as a corona which can be maintained over roughly 5.7 hr. However, observations show that coronal loops are dynamical entities which exhibit heating and cooling processes constantly. Likewise, the loops with a collapsing corona obtained here exhibit heating events with nanoflare-like temperatures constantly, which can match the observed bursty X-ray intensity profiles and the statistics displaying a power-law distribution of the heating events (cf. Paper 1). Also, a loop that is visible in soft X-rays over a large period of time may in fact result from the effect of different threads in the loop being heated at different times, thus giving the impression of a steady and uniformly heated loop (as discussed in Petsourakos & Klimchuk 2009). In the simple model we have considered, we have assumed that the heating acts uniformly along the radial direction, thus disabling the possibility of many threads being heated at different times. We thus cannot completely reject the possibility of Alfvén waves heating the coronae of short and thin loops. This idea should however be tested in an extended (at least 2.5 dimensional) version of this model.

All coronae show a range of velocities for which they are stable throughout the simulation and for which their lengths are constant. However, when the photospheric velocity field exceeds a critical value, the corona collapses. The critical velocity is dependent on the parameters of the model. In this regime, wave heating can no longer account for the large cool mass flux from the increasing wave amplitudes and collapses. Generally, the collapse is not due to a local increase in the corona of the radiative losses from the formation of a cool condensation as in the case of catastrophic cooling (Antiochos et al. 1999), and does not exhibit “limit cycles” (Müller et al. 2003). The later are characteristic of the catastrophic cooling mechanism which is proposed as an explanation for coronal rain. Further research in that direction shows that Alfvén waves are unable to reproduce the observed coronal rain due to their characteristic uniform heating, thus proposing coronal rain as a marker for coronal heating mechanisms (Antolin & Shibata 2009).

All of the obtained coronae are uniformly heated irrespective of the parameters in the model. This is a characteristic of Alfvén wave heating. The distribution of the heating in coronal loops as derived from observations is a matter of debate. Indeed, different methods for the analysis of observational data may lead to different results. A famous example of this fact is the analysis of the data set from soft X-ray observations with the Yohkoh/SXT instrument. An interpretation of the heating distribution of the observed loops in terms of apex concentrated heating (Reale 2002), footpoint concentrated heating (Aschwanden 2001b), and uniform heating (Priest et al. 1998) has been given. There seems to be however more observational evidence of coronal loops being heated toward the footpoints in active regions (Aschwanden 2001a; Aschwanden et al. 2000). Further evidence of this fact has been found by Hara et al. (2008) using the Hinode/EIS instrument, in which active region loops are shown to exhibit upflow motions and enhanced nonthermal velocities in the hot lines of Fe xiv 274 and Fe xv 284. Possible unresolved high-speed upflows were also found. In Paper 1, we found that footpoint or uniform nanoflare heating exhibits hot upflows, thus fitting in the observational scenario of active regions, while Alfvén wave heating was found to exhibit hot downflows, which may fit in the observational scenario of quiet-Sun regions (Chae et al. 1998; Brosius et al. 2007). The uniform heating from Alfvén waves further supports this conclusion, since it is a characteristic of loops more generally found in quiet-Sun regions. Active region loops exhibit low-expansion factors due to the high magnetic field filling factor in those regions. In this chapter, we have found that Alfvén wave heating is effective only in thick loops (with area expansions between the photosphere and corona higher than 600), further emphasizing our conclusion that active regions may not be heated by Alfvén waves. These results seem to point to an important role of Alfvén wave heating in quiet-Sun regions, where loops are often long and more expanded than in active regions, and kG (or higher) bright points are ubiquitous.

Another important result we have found is that both long- (above 100 s) and short-period (below 50 s) waves (where the period is the resulting period of the longitudinal modes from mode conversion; the period of the Alfvén waves is twice the stated period) play an important role in the heating of the loops. Long-period waves produce very hot heating events in the corona and thus increase the average temperature of the corona due to the strong shocks they produce. Short-period waves are responsible for keeping the corona, thus making it stable through uniform heating from the numerous weak shocks they produce. We have therefore a compromise between long- and short-period waves leading to efficient Alfvén wave heating. The 300 s period waves are found to have considerable power to heat the corona even with low photospheric velocity amplitudes of $\sim 0.2$ km s$^{-1}$. For these waves, resonances seem to be triggered in the loop, which allow higher transmission from the waves into the corona and subsequent mode trapping leading to efficient dissipation. This resonant damping mechanism is however not observed for random wave generation (white-noise spectrum) or with other geometric parameters for the loop. A thorough study of these coronal resonances for Alfvén waves will be the subject of a future paper.

P.A. thanks M. Carlsson, V. Hansteen, L. Heggland, E. Leer, R. Erdélyi, T. Matsumoto, K. Ichimoto, T. Suzuki, and H. Isobe for many fruitful discussions. P.A. acknowledges S. F. Chen for patient encouragement. This work was supported by the Grant-in-Aid for the Global COE Program “The Next Generation of Physics, Span from Universality and Emergence” from the Ministry of Education, Culture, Sports, Science, and Technology (MEXT) of Japan, by a grant from the International Astronomical Union, and by a Grant-in-Aid for Creative Scientific Research, “The Basic Study of Space Weather Prediction” (17GS0208; Head Investigator: K.S.), from the Ministry of Education, Science, Sports, Technology, and Culture of Japan. The numerical calculations were carried out on Altix3700 BX2 at YITP in Kyoto University.
REFERENCES

Anderson, L. S., & Athay, R. G. 1989, ApJ, 336, 1089
Antiochos, S. K., MacNeice, P. J., Spicer, D. S., & Klimchuk, J. A. 1999, ApJ, 512, 985
Antolin, P., Shibata, K., Kudoh, T., Shiota, D., & Brooks, D. 2008, ApJ, 688, 669
Antolin, P., & Shibata, K. 2009, arXiv:0910.2383
Antolin, P., Shibata, K., Kudoh, T., Shiota, D., & Brooks, D. 2009, arXiv:0903.1766
Aschwanden, M. J. 2001a, ApJ, 560, 1035
Aschwanden, M. J. 2001b, ApJ, 559, L171
Aschwanden, M. J. 2004, Physics of the Solar Corona. An Introduction (Chichester, UK: Praxis Publishing Ltd)
Aschwanden, M. J., & Nightingale, R. W. 2005, ApJ, 633, 499
Aschwanden, M. J., Nightingale, R. W., & Alexander, D. 2000, ApJ, 541, 1059
Banerjee, D., Erdélyi, R., Oliver, R., & O’Shea, E. 2007, Sol. Phys., 246, 3
Brosius, J. W., Rabin, D. M., & Thomas, R. J. 2007, ApJ, 656, L41
Chae, J., Yun, H. S., & Poland, A. I. 1998, ApJS, 114, 151
Cranmer, S. R., van Ballegooijen, A. A., & Edgar, R. J. 2007, ApJS, 171, 520
De Pontieu, B., et al. 2007, Science, 318, 1574
De Pontieu, B., & Ballai, I. 2007, Astron. Nachr., 328, 726
Erdélyi, R., & Fedun, V. 2007, Science, 318, 1572
Erdélyi, R., & Goossens, M. 1995, A&A, 294, 575
Evans, C. R., & Hawley, J. F. 1988, ApJ, 332, 659
Goldstein, M. L. 1978, ApJ, 219, 700
Golub, L., et al. 2007, Sol. Phys., 243, 63
Hara, H., et al. 2008, ApJ, 678, L67
Heggland, L., De Pontieu, B., & Hansteen, V. H. 2009, ApJ, 702, 1
Heyvaerts, J., & Priest, E. R. 1983, A&A, 117, 220
Hollweg, J. V. 1984, ApJ, 277, 392
Hollweg, J. V., Jackson, S., & Galloway, D. 1982, Sol. Phys., 75, 35
Hori, K., Yokoyama, T., Kosugi, T., & Shibata, K. 1997, ApJ, 489, 426
Houston, M. S. 1991, Sol. Phys., 133, 357
Kiseleva, O., & Priest, E. R. 1994, A&A, 300, 232
Kudoh, T., Matsumoto, R., & Shibata, K. 1998, ApJ, 514, 493
Landini, M., & Monsignori Fossi, B. C. 1990, A&AS, 82, 229
Mendoza-Briceño, C. A., Sigalotti, L. D. G., & Erdélyi, R. 2005, ApJ, 624, 1080
Moore, R. L., Tasker, E. J., & An, C.-H. 1991, ApJ, 378, 347
Moriyasu, S., Kudoh, T., Yokoyama, T., & Shibata, K. 2004, ApJ, 601, L107
Müller, D. A. N., Hansteen, V. H., & Peter, H. 2003, A&A, 411, 605
Muller, R., Roudier, T., Vigneau, J., & Auffret, H. 1994, A&A, 283, 232
Nakariakov, V. M., & Verwichte, E. 2005, Living Rev. Sol. Phys., 2, 3
Ofman, L., & Aschwanden, M. J. 2002, ApJ, 576, L153
Parker, E. N. 1991, ApJ, 372, 719
Patsourakos, S., & Klimchuk, J. A. 2009, ApJ, 696, 760
Poedts, S., Goossens, M., & Kuper, W. 1989, Sol. Phys., 123, 83
Priest, E. R., et al. 1998, Nature, 393, 545
Reale, F. 2002, ApJ, 580, 566
Rosner, R., Tucker, W. H., & Vaiana, G. S. 1978, ApJ, 220, 643
Routh, S., Musielak, Z. E., & Hamer, R. 2007, Sol. Phys., 246, 133
Ruderman, M. S., Berghmans, D., Goossens, M., & Poedts, S. 1997, A&A, 320, 305
Ruderman, M. S., & Erdélyi, R. 2009, Space Sci. Rev., 149, 199
Serio, S., Peres, G., Vaiana, G. S., Golub, L., & Rosner, R. 1981, ApJ, 243, 288
Shibata, K., Tajima, T., Steinolfson, R. S., & Matsumoto, R. 1989a, ApJ, 345, 584
Shibata, K., et al. 1989b, ApJ, 338, 471
Solanki, S. K. 1993, Space Sci. Rev., 63, 1
Sterling, A. C., Shibata, K., & Mariska, J. T. 1993, ApJ, 407, 778
Stone, J. M., & Norman, M. L. 1992, ApJS, 80, 791
Suzuki, T. K., & Inutsuka, S.-i. 2006, J. Geophys. Res. (Space Physics), 111, A06101
Takeuchi, A., & Shibata, K. 2001, ApJ, 546, L73
Taroyan, Y. 2008, in IAU Symp. 247, Waves & Oscillations in the Solar Atmosphere: Heating and Magneto-Seismology, ed. R. Erdélyi & C. A. Mendoza-Briceno (Cambridge: Cambridge Univ. Press), 184
Taroyan, Y., & Erdélyi, R. 2009, Space Sci. Rev., 149, 229
Terasawa, T., Hoshino, M., Sakai, J.-I., & Hada, T. 1986, J. Geophys. Res., 91, 4171
Tomczyk, S., et al. 2007, Science, 317, 1192
Tsuneta, S., et al. 2008, ApJ, 688, 1374
Uchida, Y., & Kaburaki, O. 1974, Sol. Phys., 35, 451
Van Doorsselaere, T., Nakariakov, V. M., & Verwichte, E. 2008, ApJ, 676, L73
Verth, G., Erdélyi, R., & Goossens, M. 2009, ApJ, submitted
Verth, G., Erdélyi, R., & Goossens, M. 2010, ApJ, submitted
Wentzel, D. G. 1974, Sol. Phys., 39, 129
Williams, D. R. 2004, in SOHO 13, Waves, Oscillations and Small-Scale Transients Events in the Solar Atmosphere: Joint View from SOHO and TRACE, ed. H. Lacoste (ESA SP-547; Noordwijk: ESA), 513
Yabe, T., & Aoki, T. 1991, Comput. Phys. Commun., 66, 219
Yokoyama, T. 1998, in Solar Jets and Coronal Plumes, ed. T.-D. Guyenne (ESA SP-421; Paris: ESA), 215
Zaqarashvili, T. V. 2003, A&A, 399, L15