Abstract: Herein, we propose a nano displacement sensor based on the interface state of a terahertz hetero-structure waveguide. The waveguide consists of two periodically corrugated metallic tubes with different duty ratios, which can result in similar forbidden bands in their frequency spectra. It was found that the topological properties of these forbidden bands are different, and the hetero-structure can be formed by connecting these two waveguides. In the hetero-structure waveguide, the interface state of an extraordinary transmission can always arise within the former forbidden bands, the peak frequency of which is highly dependent on the cavity length at the interface of the two periodic waveguides. So, by carefully designing the structure's topological property, the hetero-structure waveguide can be efficiently used to produce a displacement sensor in the THz frequency range. The simulations show that the resolution of the displacement can be as small as 90 nm and the sensitivity can reach over 1.2 GHz/µm. Such a sensitive interface state of the proposed hetero-structure waveguide will greatly benefit THz applications of functional devices, including not only displacement sensors but also switches with high extinction ratios, tunable narrow-band filters, and frequency division multiplexers.

Keywords: resonances; periodic waveguides; reflection phases; topological properties

1. Introduction

In recent years, with the development of ultra-fast technologies, the research on terahertz (THz) technology has seen unprecedented progress [1–4]. THz waves have many unique advantages over the electromagnetic waves in the other bands, which allow THz technology to have considerable applications in some important areas, such as military, astronomy, radar, and medicine [5–8]. Due to its strong penetrability and low photonic energy, THz imaging technology will replace X-rays in medical examinations and will not cause harm to the human body [9]. It can also be used for detection in complex environments and identification of plastic weapons [10]. The characteristic spectra of many biomolecules and chemicals are also located in the THz band, including many drugs. So, it is also useful to employ THz waves in substance identification and biomedical research [11]. The broadband characteristics of THz waves result in their predictable applications in communication fields, and their wireless transmission speed can reach tens of Gb/s [12,13]. In the upcoming 6G Internet of Things, THz waves are also considered to be good candidates in short-range, bandwidth-aggressive services such as in the smart home scenario [14]. In THz systems, functional devices are essential to applications,
including, of course, displacement sensors. For example, in THz imaging, displacement sensing can correct the errors of relative motion between objects and probes, and it is expected to be adopted in calibrating the amplitude of characteristic peaks for different substances. In this era of interconnection of all things, most communications depend on THz waves, and displacement sensors can be integrated into smart devices to monitor and control their position changes.

The micro–nano displacement sensor as a device for high-precision monitoring has been used in automotive industry [15], small-scale manipulation [16,17], construction [18,19], micro-grippers [20], physiological sensing [21,22], and so on. The micro–nano displacement sensing technology of the communication optical band has been developed over many years, including plasmonic slot metamaterials [23], Fabry–Pérot interferometers [24], photonic crystal fibers [25], and so on. In 2011, Liu et al. reported a sensing structure with double-fiber Bragg gratings [26]. In 2014, Qu et al. presented an interferometric fiber-optic bending/micro-displacement sensor based on a plastic dual-core fiber with one end coated by a silver mirror [27]. In 2016, Gao et al. realized an optical displacement sensor based on anti-resonant reflecting guidance in a capillary covered hollow-core fiber [28]. However, a THz micro–nano displacement sensor of waveguide types that can be applied in THz systems without additional optical devices has not been reported yet. It will be very intriguing to realize THz micro–nano displacement sensing with high precision, small size, and easy integration. Hypersensitive THz displacement sensors could expand the applications of THz technology and pave the way for THz micro–nano positioning in the future smart life of all things connected.

Here, we propose a THz displacement sensor based on the hetero-structure waveguide, which can provide a sensitive spectrum response to a tiny displacement. Hetero-structures consist of semiconductor materials with different forbidden bands [29–31], which have been developed for artificial structures for years [32–36]. Further, the waveguides in the THz frequency range have been investigated numerically for functional devices [37,38]. The proposed hetero-structure contains a cylindrical waveguide with two different periodic corrugations on the wall. Based on their different topological properties, these two periodicities are used to generate an interface state, which can be recognized by a very narrow transmitted peak in its spectrum. It was found that the transmitted peak highly depends on the cavity length at the interface of two periodicities. Increasing the cavity length can result in red shift of the peak, which is very promising for use in fabricating a sensitive THz sensor. In the following section, the hetero-structure waveguide and its arising interface state are demonstrated. There is a transmitted peak arising in the former forbidden band due to the interface of the two periodic structures. The hetero-structure waveguide composed of two opaque periodic tubes become transparent at a certain frequency. The different topological properties of the two periodic structures can be explained by their reflection phases at the interface. The displacement THz sensor is proposed in Section 3 and the sensing performance is discussed in detail. Finally, the major findings about the super-high resolution and sensitivity are summarized.

2. Hetero-Structure Waveguides

Hetero-structure waveguides are usually combinations of multiple different tubes with unequal topological band gaps. Between each waveguide of the hetero-structures, interface states can always arise to produce an extraordinary transmitted peak in the former forbidden bands of periodic waveguides, which is very promising for high-resolution sensing due to its very narrow line width. Here, we propose a very simple corrugated waveguide system to demonstrate a THz micro–nano displacement sensor with very high precision. In waveguides with periodic wall corrugations, frequency gaps will appear around the resonant frequencies, in which the electromagnetic waves cannot pass through the structures. Bragg resonance will happen when the longitudinal wavenumbers of the same transverse modes satisfy the matching condition [39]. Connecting two periodic waveguides with similar Bragg gaps can result in an interface state with a very sharp transmitted peak in the overlapping frequency band gap when their topologies are different. These two waveguides have the same average radius $r_0$ and period $\Lambda$, the transmission spectra and geometry structures of which are
shown in Figure 1a–c. The duty ratio refers to the proportion of wide radius part in a period length, and it has been proved that different duty ratios can introduce different topological band gaps [40]. We selected different duty ratios 0.8 and 0.4 for Waveguides A and B, respectively, to achieve the different topologies.

In a hollow metallic cylindrical periodic waveguide, the lowest-order Bragg resonance happens at

$$f_r = \frac{c}{2\pi} \sqrt{\frac{k_r^2}{r_0^2} + \left(\frac{\pi}{\Lambda}\right)^2}$$

for transverse magnetic (TM) waves with $k_r = 2.4048$. To set the Bragg resonance around 1 THz, we selected the geometry parameters of the periodic waveguides as $R_I = 220 \mu m$, $R_{II} = 180 \mu m$, and $\Lambda = 183 \mu m$ with $r_0 = (R_I + R_{II})/2 = 200 \mu m$, where $R_I$ and $R_{II}$ are the wide and narrow radii of the structures, respectively. The hetero-structure waveguide was obtained by directly connecting the wide tube of Waveguide A and the narrow tube of Waveguide B.

We employed finite element method simulations on the waveguide structures with an axisymmetric model in COMSOL Multiphysics software. In the simulations, the refractive index of inside air was set to be 1, and perfect electrical boundary conditions were assigned to the walls of these three waveguides. As the THz source, a first-order TM mode was excited at the inlet of each waveguide, and the radiation condition was assigned to the outlet boundary. The 0.8–1.1 THz frequency range was selected with a step of 0.001 THz, and the electromagnetic fields were calculated in the whole waveguide.

Figure 1. Transmission spectrum and electric field $E_z$ components of Waveguides A, B, and the hetero-structure of their combination. (a) The blue dash–dot, green dash, and red solid lines are the transmission spectra of Waveguides A and B and the hetero-structure, respectively. The electric fields $E_z$ of Waveguides A (b) and B (c) and the hetero-structure (d) at 1.027 THz illustrate the energy attenuation and localization at the interface of the structure. The electric fields were normalized by their own maximum in each waveguide.
Defining the transmission coefficient $T$ as the ratio of optical powers of the outlet and inlet, we calculated the transmission spectra of Waveguides A and B and the hetero-structure waveguide, and depicted them by the dash–dot, dashed, and solid lines in Figure 1a. It shows that Waveguide A has a band gap around 0.838–1.038 THz, and Waveguide B’s is around 0.848–1.051 THz. The smaller duty ratio of Waveguide B leads to a small frequency shift of the whole Bragg gap to a higher frequency. However, these two waveguides have a common forbidden band in the frequency range of 0.848–1.038 THz, in which the THz radiation cannot pass through either Waveguide A or B. The frequency of 1.027 THz falls in this common forbidden band—that is to say, a THz wave at this frequency cannot pass through either of these two waveguides—but what a surprise that we find an extraordinary transmitted peak with a center frequency of 1.027 THz in the spectrum of the hetero-structure waveguide. The forbidden band becomes much wider than that of either of the two waveguides.

To verify the interface state arising, we also simulated the electric field distributions for these three different waveguides, and the $E_z$ components of the electric fields at 1.027 THz are depicted in Figure 1b–d for Waveguides A and B and the hetero-structure, respectively. The electric fields were normalized by their own maxima in the figure. The THz waves enter the waveguide from the bottoms of Waveguides A and B in Figure 1b,c respectively. It can be observed that the THz wave decays along the direction of propagation. Fortunately, the frequency is very close to the edge of the forbidden bands. So, we find that Waveguide B with a smaller duty ratio is much more effective for THz attenuation. In any case, the THz radiation at 1.027 THz cannot pass through either Waveguide A or B. When we connect these two waveguides and excite a THz wave with the first TM mode at the left side of the hetero-structure waveguide, as shown in Figure 1d, the situation turns out to be totally different. The THz waves accumulate around the interface of Waveguides A and B, which is known as the interface state. Due to the energy accumulation, the former opaque waveguides become transparent to a special frequency THz wave, as shown in Figure 1a. It is because of the normalization to the maximum electric field that the $E_z$ component at the outlet is smaller than 1. Based on the transmission spectrum and the electric field distribution, we confirm the interface state arising in the proposed hetero-structure waveguide.

The remarkable transmission feature is due to the different topological properties of the two waveguides, which can be identified by the Zak phases of the two Bragg bands [40]. It is also more convenient to investigate the reflection phase of each waveguide at the interface. If the phases have the same sign, the related Bragg gaps are of a similar topology. Otherwise, they are topologically different, and the interface state arises.

To achieve the reflection phase of each waveguide, we connected a straight tube to the corrugated one and simulated the $E_z$ component of electric fields with an incident TM mode from the straight tube at 1.027 THz. A straight tube with a length of 1000 µm and radius of 200 µm was connected to the wide radius port of Waveguide A. For Waveguide B, it was connected to the narrow radius port. Thus, the reflection properties at the interface of each waveguide could be observed. The same straight tube with a perfect electrical boundary at the other end was also simulated for reference. The reflected components of the electric fields are shown in Figure 2a–c for Waveguide A, the perfect electrical boundary, and Waveguide B, respectively. For convenience, we also depict the amplitude of $E_z$ by solid lines. With the aid of the added dashed line, we can conclude that the reflection phase of Waveguide A is delayed while that of Waveguide B is advanced when considering the perfect electrical boundary reference as a zero-phase case. The reflection phases of Waveguides A and B have opposite signs, indicating the topological difference of the two Bragg gaps. So, the interface state arises at 1.027 THz, where we found a narrow transmitted peak in the spectrum. Such an extraordinary peak with very narrow line width would be a good candidate for THz sensing applications.
Figure 2. $E_z$ components of reflected electric fields at 1.027 THz for (a) Waveguide A, (b) the perfect electrical boundary, and (c) Waveguide B. The reflected phase of Waveguide A is delayed while that of Waveguide B is advanced relative to the THz waves reflected by the perfect electrical boundary.

3. Micro–Nano Displacement Sensing

To realize micro–nano displacement sensing, we propose the hetero-structure waveguide (Figure 3a) composed of two tubes with average inner radius 200 $\mu$m and period 183 $\mu$m based on the above analysis. The tube wall is suggested to be 10 $\mu$m thick silver (Ag), which has low loss in the THz frequency range. So, the outer radii are 190 $\mu$m and 230 $\mu$m for the narrow and wide parts, respectively. According to the duty ratios, the lengths of the wide and narrow tubes are 146.4 $\mu$m and 36.6 $\mu$m, respectively, for Waveguide A, whereas they are 73.2 $\mu$m and 109.8 $\mu$m for Waveguide B. To fabricate an integrated device, we have to increase the length of the wide tube at the right end of Waveguide A and add a ring at the left end of Waveguide B. The increased length is 276 $\mu$m and the outer radius of the ring should be 220 $\mu$m to make sure that they can be connected. The length can be mechanically changed within the range of 20–120 $\mu$m. Although the measurement cannot start from 0 $\mu$m due to the length of the narrow tube in Waveguide B, the measurement range of displacement can still reach 100 $\mu$m. The number of periods in each waveguide is 5.

We also performed simulations on different combinations of duty ratios. The duty ratios of Waveguides A and B were selected from 0.1 to 0.9 in intervals of 0.1. The results show that all connections of different duty ratios can create a similar extraordinary transmitted peak, that is to say, the interface state between the two periodic waveguides always arises in the former Bragg gaps due to the different topologies. However, the bandwidth and frequency shift of the peaks highly rely on the duty ratios. Only the duty ratio combination of 0.8 and 0.4 can result in the narrowest bandwidth and maximum displacement, which could be of extreme benefit for practical applications. So, the proposed structure with duty ratios 0.8 and 0.4 was analyzed in detail for THz displacement sensing.

In the displacement sensing, we first fix Waveguide A, then adjust the Waveguide B to a relative position to be measured, and finally fix Waveguide B to that position. In this way, Waveguide B
moves relative to Waveguide A, which increases the length of the cavity between the two waveguides. The THz wave is incident from the narrow radius of Waveguide A and emitted from the wide radius of Waveguide B. The frequency of the transmitted peak shifts with the displacement, so that the hetero-structure waveguide realizes displacement sensing. The simulated transmission for different displacements is depicted in Figure 3b by different lines. The center frequency of the transmitted peak is 1.002 THz when the displacement is 20 µm in the hetero-structure waveguide. When Waveguide B moves away from Waveguide A, the length of the middle cylindrical waveguide increases and the peak frequency shifts to the low frequency range. All the transmissions are above 0.85, and the highest transmission of 0.948 is obtained when the displacement is 120 µm.

To measure the displacement by THz waves, we define the frequency shift \( \Delta f \) from the frequency of 1.026 THz at 0 µm. The former peak moves from 1.027 THz to 1.026 THz for the 0 µm waveguide because the real dielectric constant of Ag is considered in the simulations. The frequency shift \( \Delta f \) according to the displacement is marked in Figure 3c by the circles, and we performed a linear fit (the dashed line) as follows:

\[
\Delta f = -1.260 \times L
\]
where $L$ is the displacement in micrometers, and the frequency shift is in gigahertz. The fitting results show that when the hetero-structure waveguide is stretched 1 µm, the transmitted peak moves 1.260 GHz to a lower frequency. When $L = 80$ µm, the narrowest bandwidth is 2.580 GHz, and when $L = 20$ µm, the maximum bandwidth is 4.610 GHz. The maximum displacement that can be measured by the hetero-structure waveguide is 100 µm, the adjustable range of frequency is 0.877–1.002 THz, and the whole bandwidth is 124.5 GHz. So, the sensitivity of such a waveguide-type sensor can reach over 1.2 GHz/µm, and the minimum resolvable length is 2.073 µm when the displacement $L$ is around 80 µm.

To realize the proposed structure, there are two ideas for fabrication. The first idea is to make a hollow metallic waveguide with substrates outside, as shown in Figure 4a. The deep lithography process can be employed to machine two half-cylinder polymers, and the metallic materials, such as Ag, can be sputtered on the two parts. To form the tube, we can hold the two parts together and eliminate a thin layer at the end of Waveguide B. The second idea is to produce a corrugated polymer core by 3D printing, as shown in Figure 4b. The two structures both end at the narrow radius parts. A silver film can be coated on the surface of the corrugated core, and a capillary coated with a silver film inside can be used to connect the two waveguides. Thus, the shifting parts are still hollow. When the proposed structure is ready, Waveguides A and B can be fixed to the two holders using epoxy glue [28]. With the aid of a 3D nano-positioning stage or optical micromanipulation, we can assemble the sensor to the test structures or THz systems.

Figure 4. Sketch maps of the device fabrication process with the substrates outside (a) or inside (b).

The number of periods is also an important parameter for the hetero-structure waveguide sensor and can directly affect its resolution. Here we studied the effects of the number of periods on the sensing performance. The number of periods of the two waveguides takes the same value and is denoted by $N$. The value of $N$ ranges from 4 to 9, while the length $L$ is fixed at 80 µm. The transmission spectra and the measurement resolutions of the micro–nano displacement sensor are shown in Figure 5a,b, respectively, in the cases of different $N$. The bandwidth becomes extremely narrow as the number of periods increases, but when the number of periods is greater than 8, the transmission gets a little bit smaller. When $N = 9$, the transmission is just over 0.2. When the number of periods is smaller than 7, the transmissions are all greater than 0.5. The variation of the measurement resolution according to
the number of periods $N$ for the hetero-structure sensor is also depicted in Figure 5b by the crosses, with its fitting curve (the solid line) as

$$Rs = 7063 \times N^{-5.083}$$

Figure 5. Transmitted peaks (a) and measurement resolutions (b) for different numbers of periods.

The resolution of the sensor is defined as its smallest measurable displacement, which is inversely proportional to the fifth power of $N$. When increasing the number of periods, we can greatly improve the performance of the sensor. The resolution reaches 282 nm for $N = 7$, while it gets as small as 90 nm for $N = 9$. The related sensitivity is over 1.2 GHz/µm. This is a highly sensitive THz nano displacement sensor that can be used in various applications involving accurate displacement measurements. It can also be extended to a wider range of applications when cascade hetero-structure waveguides are considered.

Through simulation of the hetero-structure waveguide, it was proved that the structure can produce a very narrow THz pulse. By changing the connection length between Waveguides A and B, the frequency of the transmitted peak moves towards the low frequency range, thus determining the micro–nano displacement sensing function of the proposed structure in the THz region. For measuring car body paints, a THz transceiver was mounted on a robot [41]. The proposed sensor can be integrated to monitor tiny movements of the mechanical arms without any additional sources. Based on the recorded THz data, the extracted layer thickness can be corrected. In the Internet of Things, THz functional devices play a key role in communication and intelligence applications [42]. The integrated displacement sensor can not only provide more accurate locations of communication...
nodes, but also monitor subtle changes of smart terminals. The structure design and performance simulations confirmed THz displacement sensing based on the hetero-structure waveguide.

4. Conclusions

We proposed a micro–nano displacement sensor based on hetero-structure waveguides in the THz frequency range. It is composed of two periodically corrugated waveguides that have similar Bragg forbidden bands. The THz waves cannot pass through either of these two periodic waveguides in the common frequency range of 0.848–1.038 THz. The topological analysis indicates that the Bragg gaps can present different topological properties, which can create an interface state with a very sharp transmitted peak in the THz spectrum when these two periodic waveguides are connected. Due to the topological difference of the Bragg gaps, the hetero-structure waveguide turns transparent at a certain frequency, where both the waveguides are otherwise opaque. Based on the interface state’s induced transmission, we proposed a THz micro–nano displacement sensor by carefully connecting two corrugated waveguides. When the two waveguides are held by different structures, their relative displacement can be achieved by measuring the shift of transmission peaks, and the resolution can be improved by increasing the number of periods. The proposed hetero-structure waveguide-type sensor has excellent performance, such as a wide measurable range of 100 µm, minimum resolution of 90 nm, and maximum sensitivity of over 1.2 GHz/µm, which allow it various applications in many fields, such as chemical and biomedical sensing, micro-manipulation, imaging, and intelligent control. Besides displacement sensing applications, the proposed interface state of the hetero-structure waveguide can also be applied to other functional devices, such as switches, filters, and frequency division multiplexers.

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