Online Rotor and Stator Resistance Estimation Based on Artificial Neural Network Applied in Sensorless Induction Motor Drive

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Abstract: This paper presents a new approach method for online rotor and stator resistance estimation of induction motors using artificial neural networks for the sensorless drive. In this method, the rotor resistance is estimated by a feed-forward neural network with the learning rate as a function. The stator resistance is also estimated using the two-layered neural network with learning rate as a function. The speed of the induction motor is also estimated by the neural network. Therefore, the accurate estimation of the rotor and stator resistance improved the quality of the sensorless induction motor drive. The results of simulation and experiment show that the estimated speed tracks the real speed of the induction motor; simultaneously, the error between the estimated rotor and stator resistance using neural network and the normal rotor and stator resistance is very small.

Keywords: rotor resistance estimation; stator resistance estimation; sensorless control; artificial neural network (ANN); indirect field-oriented control (IFOC)

1. Introduction

The problem of the sensorless indirect rotor flux control of induction motor (IM) is an important aspect in the study of induction motor drive systems [1]. In the sensorless control of a vector controlled three-phase induction motor drive, the rotor flux angle depends on the rotor resistance [2–5]. On the other hand, the rotor flux estimation is sensitive to the changes in the rotor and the stator resistance, especially in the case of the low rotational speed; the speed estimation of an induction motor again depends on the estimated rotor flux [6]. Therefore, the accuracy of the estimated rotor and stator resistance will improve the accuracy of the estimated speed and the estimated rotor flux, thereby improving the quality of the sensorless drive control [7]. In the operation of induction motor drives, the rotor resistance can vary up to 100% due to changes in temperature and rotor speed, so obtaining this information through a thermal model or temperature sensors is very difficult, especially for induction motors [8].

The rotor resistance estimation algorithms have been widely studied in the literature. The well-known approaches in recent studies are based on the following:

• Model Reference Adaptive System (MRAS) [9–11],

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• Extended Kalman Filters [12–14];
• Sliding Mode Control [15,16];
• Fuzzy Logic Technique [17,18].

However, recently, different combinations and modifications have also been proposed. Interesting examples include the following:

• One article [19] concerns a sensorless control approach for a five-phase induction motor drive. The sensorless scheme uses the sliding mode theory, which applies a sliding mode observer to estimate rotor resistance. The operation methodology of the proposed control technique is formulated using the mathematical model of the machine and the two-time-scale approach.
• The author of [20] proposes the combination of parameter estimation-based observers with the dynamic regression extension and mixing parameter adaptation. The first framework is used to recast the flux observation task as a parameter estimation problem, for which the dynamic regressor extension and mixing method (DREM) technique is applied.
• One article [21] proposes using carrier signal injection with minimized torque ripple for rotor resistance estimation. The proposed approach is based on the injection of a relatively low-frequency carrier signal into the reference of the rotor flux linkage magnitude as well as extraction of the induction machine’s response to the carrier signal, which is then used in a model reference adaptive system.
• The author of [22] proposes the verification of rotor resistance identification in the field-oriented control-based drive system using the slip ring machine-based test bench. The paper proposes the torque calculations using the current stator and flux to propose the model reference adaptive system for online estimation of rotor resistance (without injection of the signal).
• Other articles [23,24] propose an online estimated rotor resistance method using a neural network. However, the proposed method is still limited by the learning rate that is pre-selected and does not change during the rotor resistance estimation process. Therefore, if the learning rate is selected inappropriately, it will lead to a slow network training process and large network output errors. The choice of appropriate learning rate is mainly based on the experience of the researchers.

The literature also proposes several approaches to stator resistance estimation. The well-known approaches in recent studies are based on the following:

• MRAS [25–27];
• Luenberger Observer [28–31];
• Fuzzy Logic Technique [32–34];

However, recently, different combinations and modifications have also been proposed. Interesting examples include the following:

• One article [35] proposes a novel Power Quality Model Reference Adaptive System (PQ-MRAS) concept for stator resistance. It uses the active and reactive power of the machine, which is calculated using measurable signals, (e.g., stator voltage and current). The paper includes a detailed description of the proposed estimator.
• The author of [36] proposes online identification of stator resistance based on the model reference adaptive system. In the article, the backpropagation is used to define the error between the measured and estimated value of stator current to adjust the weights of the neural network.
• The author of [37] presents the IM model that is transformable into the adaptive observer form. In this method, stator resistance estimation leads to the overparameterization problem. The proposed solution uses the first-order approximation of the error dynamics to the adaptive observer.
• The online stator resistance estimation methods using a neural network were studied and performed in [38]. However, in the proposed method, the learning rate must be selected and not changed during the estimation process. Consequently, this reduces its accuracy.
In this article, the authors propose a novel method to estimate rotor resistance and stator resistance using artificial neural networks with the learning rate as a function. This is an extension of previous research seeking to improve the control quality of the sensorless induction motor drive. This paper is arranged as follows. Section 2 presents the method to estimate rotor resistance using a two-layered neural network with the learning rate as a function. In Section 3, the rotor and stator resistance estimation method by using a two-layered neural network in which the learning rate is also a function is proposed. The experimental results in Section 4 have been proven with the proposed algorithm. The rotor and the stator resistance are accurately estimated, leading to the estimated speed of the motor being very close to the real speed, thus having the potential to improve the quality of the induction motor sensorless drive system. Finally, conclusions are given in Section 5.

2. Rotor Resistance Estimation Using Artificial Neural Networks

The rotor resistance estimator structure of the induction motor is based on MRAS [1,3], presented in Figure 1.

![Rotor resistance estimator based on MRAS including a neural network trained by the error-back propagation algorithm.](image)

**Figure 1.** Rotor resistance estimator based on MRAS including a neural network trained by the error-back propagation algorithm.

The outputs of the reference model (voltage model) are components of rotor leakage flux in the static frame:

\[
\begin{align*}
\psi_{\alpha m}^r &= \frac{L_r}{L_m} \left[ \int (V_{sa} - R_s i_{sa}) dt - \sigma L_s i_{sa} \right] \\
\psi_{\beta m}^r &= \frac{L_r}{L_m} \left[ \int (V_{sb} - R_s i_{sb}) dt - \sigma L_s i_{sb} \right] \\
\end{align*}
\]

(1)

where \( \sigma = (1 - L_m^2/L_s L_r) \) — leakage coefficient.

Stator leakage flux has the following equations:

\[
\begin{align*}
\psi_{sa} &= \int (V_{sa} - R_s i_{sa}) dt \\
\psi_{sb} &= \int (V_{sb} - R_s i_{sb}) dt \\
\end{align*}
\]

(2)
Because the direct current (DC) voltage applied to the inverter is undulating, the integral stage in Equation (2) causes the stator leakage flux error. Therefore, it is necessary to adjust the stator leakage flux estimation using a multi-level low-pass filter [18]. From Equations (1) and (2), and through some transformations, we obtain equations used to estimate rotor flux according to the voltage model as follows:

\[
\begin{align*}
\psi_{ra}^{im}(k) &= \frac{L_r}{L_m^s} \psi_{sa}(k-1) - \frac{L_s L_r - L_m^2 L_m}{L_m^s} i_{sa}(k-1) \\
\psi_{rp}^{im}(k) &= \frac{L_r}{L_m^s} \psi_{sp}(k-1) - \frac{L_s L_r - L_m^2 L_m}{L_m^s} i_{sp}(k-1)
\end{align*}
\] (3)

On the other hand, the equations of the adaptive model (current model) are as follows:

\[
\begin{align*}
\psi_{ra}^{im}(k) &= W_1 \psi_{ra}^{im}(k-1) - W_2 \psi_{rp}^{im}(k-1) + W_3 i_{sa}(k-1) \\
\psi_{rp}^{im}(k) &= W_1 \psi_{rp}^{im}(k-1) + W_2 \psi_{ra}^{im}(k-1) + W_3 i_{sp}(k-1)
\end{align*}
\] (4)

where \( W_1 = 1 - \frac{T_3}{T_r}, \ W_2 = \omega_r T_s, \ W_3 = \frac{T_s}{T_r} L_m. \)

\( T_s \) is the sampling time and \( T_r = L_r / R_s \) is the rotor time constant. \( W_2 \) does not depend on the rotor time constant. It can be seen that the weights \( W_1 \) and \( W_3 \) depend on the rotor time constant. If the \( L_r \) rotor self-inductance is not changed, the weights \( W_1 \) and \( W_3 \) will be updated based on the rotor resistance to obtain high efficiency.

The two-layered neural network used to estimate rotor flux by the current model is illustrated in Figure 2.

![Figure 2](image)

**Figure 2.** Two-layered neural network used to estimate rotor flux by the current model.

The square function of rotor flux error calculated from the two models according to Equations (3) and (4) is written as follows:

\[ E_1 = \frac{1}{2} \varepsilon^2(k) = \frac{1}{2} \left( \psi_{ra}^{im}(k) - \psi_{ra}^{im}(k) \right)^2 \] (5)

The weights of the networks \( W_1, W_3 \) are obtained from the network training that minimizes the square function \( E_1 [1,9] \). \( W_1, W_3 \) are determined as follows:

\[
W_1(k) = W_1(k-1) + \eta_1 \Delta W_1(k) \quad (6)
\]

\[
W_3(k) = W_3(k-1) + \eta_3 \Delta W_3(k) \quad (7)
\]
\[ \Delta W_1(k) = -\partial E_1 / \partial W_1 = \left[ \frac{\psi^m_r(k) - \psi^m_r(k)}{\psi^m_r(k)}\right]^T \psi^m_r(k-1) \]  
\[ \Delta W_3(k) = -\partial E_1 / \partial W_3 = \left[ \frac{\psi^m_r(k) - \psi^m_r(k)}{\psi^m_r(k)}\right]^T \bar{r}_s(k-1) \]

where the learning rates \( \eta_1 \) and \( \eta_3 \) are pre-selected constants.

The problem is to replace the constant learning rate with a function so that after each update of the weight adjustment, the error \( E_1 \) value will be reduced with \( \zeta_i(k) = \Delta W_i(k) \Delta W_i(k-1) \), where the function \( \zeta_i(k) \) is the error product of the weight adjustment \( W_i \) at times \( k \) and \( (k-1) \). From this, we build the learning rate function based on the function \( \zeta_i(k) \) so that the learning rate changes in the direction of reduction of the error \( E_1 \) of the neural network. This means that if \( \zeta_i(k) \) is positive, the neural network has a slow convergence speed and must increase the learning rate; if \( \zeta_i(k) \) is negative, the learning rate must be reduced. Consider the following function:

\[ f(\zeta_i) = \text{sign}(\zeta_i) \frac{a_0}{1 + e^{-\text{sign}(\zeta_i)}} \]  

The derivative of \( f(\zeta_i) \) is \( \frac{\partial f(\zeta_i)}{\partial \zeta_i} = \frac{a_0 e^{-\text{sign}(\zeta_i)}}{(1 + e^{-\text{sign}(\zeta_i)})^2} > 0 \), where \( a_0 \) is positively identified.

Here, \( f(0) = 0 \), so \( \zeta_i(k) f(\zeta_i(k)) > 0 \) for every \( \zeta_i(k) \neq 0 \). So, the function is \( f(\zeta_i) \) congruent and homologous to the error \( \zeta_i \). Therefore, the learning rate function can be updated according to the following rules:

\[ \eta_i(k) = \eta_i(k-1) (1 + f(\zeta_i(k-1))) \]  

where \( \eta_i(k-1) \) is the learning rate at \( (k-1) \), \( \eta_i(k) \) is the learning rate at \( k \).

The learning rate determined at (11) is different from the learning rate mentioned elsewhere [1,9].

The weights of the networks \( W_1, W_3 \) are adjusted by training based on Equation (6) or (7). The rotor resistance is therefore estimated according to Equation (12) or (13) as follows:

\[ R_{r-es} = \frac{L_s(1-W_1)}{T_s} \]  
\[ R_{r-es} = \frac{L_s W_3}{L_m T_s} \]

Rotor flux estimation from Equation (1) is sensitive to changes in the stator resistance, especially in the low-speed region. Therefore, to minimize the error in the rotor resistance estimation due to the stator resistance variation, an online stator resistance estimator will be analyzed and discussed in Section 3.

3. Stator Resistance Estimation Using Artificial Neural Networks

According to [9], we have the following equation, describing components of stator currents in the static frame:

\[
\begin{aligned}
\bar{i}_{sa}(k) &= W_4 \bar{a}_{sa}(k-1) + W_5 \psi^m_{sa}(k-1) + W_6 \bar{a}_{sp}(k-1) + W_7 V_{sa}(k-1) \\
\bar{i}_{sp}(k) &= W_4 \bar{a}_{sp}(k-1) + W_5 \psi^m_{sp}(k-1) - W_6 \bar{a}_{sp}(k-1) + W_7 V_{sp}(k-1)
\end{aligned}
\]

where \( W_4 = \left[ 1 - \frac{T_s L_m^2}{\alpha L_s T_r} - \frac{T_s}{\alpha L_s} R_s \right], W_5 = \frac{T_s L_m}{\alpha L_s T_r}, W_6 = \frac{T_s}{\alpha L_s} \omega_r, W_7 = \frac{T_s}{\alpha L_s}. \)

The weights \( W_5, W_6, W_7 \) are calculated from the motor parameters, motor speed and the sampling time \( T_s \). The weighted \( W_4 \) depends on the stator resistance. The weight \( W_4 \) is the adjustment weight.
Equation (14) can be represented by two layered artificial neural networks as shown in Figures 3 and 4.

\[
E_{2} = \frac{1}{2} \varepsilon_{2}^{2}(k) = \frac{1}{2} \left( \overline{\varepsilon}(k) - \overline{\varepsilon}(k) \right)^{2} \tag{15}
\]

The weight of the network \( W_4 \) is derived from the training of the neural network so that the error square function \( E_2 \) is minimal [9]. \( W_4 \) is determined as follows:

\[
W_{4}(k) = W_{4}(k-1) + \eta_{4}\Delta W_{4}(k) \tag{16}
\]

where

\[
\Delta W_{4}(k) = -\frac{\partial E_{2}}{\partial W_{4}} = \left[ \overline{\varepsilon}(k) - \overline{\varepsilon}(k) \right]^{T} \overline{\varepsilon}(k-1) \tag{17}
\]

Similarly to the method of constructing the learning rate function to estimate rotor resistance in Section 2, the learning rate is updated as follows:

\[
\eta_{4}(k) = \eta_{4}(k-1)(1 + f(\varsigma_{4})) \tag{18}
\]
where
\[
\varsigma_4(k) = \Delta W_4(k)\Delta W_4(k-1)
\]  

(19)

The learning rate determined in Equation (18) is different from the learning rate mentioned in [6,9]. Afterward, the stator resistance can be estimated as follows:
\[
R_{s-es} = \left\{1 - W_4 - \left(\frac{T_s}{\sigma L_s}\left(1 + \frac{1}{R_{r-es}/L_s}\right)\right)\right\}(\sigma L_s/T_s)
\]  

(20)

The speed estimation used in sensorless drive in this paper is shown after [19], according to Expression (21) below:
\[
\omega_{r-es}(k) = \omega_{r-es}(k-1) + \frac{\eta_{w}}{T_s}\left(\frac{\left[\psi_{im}^\alpha(k) - \psi_{im}^\alpha(k-1)\right]}{\psi_{im}^\alpha(k-1)}\right)
\]  

(21)

where \(\eta_{w}\) is the learning rate for estimating rotor speed.

4. Results

4.1. Analysis

At the low-speed region, the rotor flux estimation from Equations (3) and (4) is very sensitive to stator and rotor resistance [9]. Therefore, online rotor and stator resistance estimation in Sections 2 and 3 will improve the quality of the sensorless drive control, especially for low speeds. A diagram of the IFOC (indirect field-oriented control) sensorless drive with online rotor and stator resistance estimation is shown in Figure 5.

![Diagram of indirect field-oriented control (IFOC) sensorless drive with online rotor and stator resistance estimation.](image)

Figure 5. Diagram of indirect field-oriented control (IFOC) sensorless drive with online rotor and stator resistance estimation.

4.2. Results of the Simulation

To simulate a sensorless drive system with rotor and stator resistance estimation, the authors used MATLAB/Simulink software (2019a, MathWorks, Natick, MA, USA).
The rotor resistance of the induction motor varies from 1.84 to 2.76 Ω, thus leading to a discrepancy between the actual rotor and stator resistance values and real values. The rotor resistance of the induction motor varies from 1.84 to 2.76 Ω, the stator resistance of the motor varies from 1.99 to 2.99 Ω (simulation process duration 0–9 s); load $T_L = 2.0$ Nm is applied at time $t = 1.5$ s. The induction motor parameters are given in Table 1.

Table 1. Induction motor parameters—Siemens (1LA 7096-2AA60-Z).

| No | Parameters            | Values       |
|----|-----------------------|--------------|
| 1  | Rated power           | 2.2 kW       |
| 2  | Rated voltage         | 400 V        |
| 3  | Rated frequency       | 50 Hz        |
| 4  | Stator resistance     | 1.99 Ohm     |
| 5  | Rotor resistance      | 1.84 Ohm     |
| 6  | Magnetizing inductance| 0.37 H       |
| 7  | Poles                 | 2            |
| 8  | Rated speed           | 2880 Rpm     |
| 9  | Rotor moment of inertia| 0.002159 kgm²|

4.2.1. Speed of Induction Motor without Rotor and Stator Resistance Estimation

Assuming that the rotor resistance increases from 1.84 to 2.76 Ω, from 0–2 s, it remains 1.84 Ω; in 2–7 s, it increases from 1.84–2.76 Ω; at 7–9 s, the rotor resistance is 2.76 Ω. The stator resistance varies from 1.99 to 2.99 Ω for 0–2 s, it remains 1.99 Ω, at 2–7 s and it increases from 1.99–2.99 Ω for 7–9 s then stays at 2.99 Ω, but the rotor and stator resistances set for the controller retain their rated resistance values. Figure 6a indicates reference speed and estimated speed throughout the simulation time. In Figure 6b, the stator and rotor resistance values differ by 50% from the initial cold resistance values; the average estimated speed is still 20 rad/s but the pulsation of the speed is nearly 0.3 rad/s.

![Figure 6](a)  ![Figure 6](b)

Figure 6. Speed of induction motor without online rotor (a) and stator resistance (b) estimation: reference speed, real speed and estimated speed.

4.2.2. Speed of Induction Motor with Online Rotor and Stator Resistance Estimation

The simulation results in Figure 7a,b show that, with the resistance estimation algorithms proposed in Sections 2 and 3, the rotor and stator resistance were accurately estimated with very small error compared to real resistance values. On the other hand, the accurate estimation of rotor and stator resistances improved the estimation of the real speed of the rotor (Figure 8), thereby improving the quality of the sensorless drive system.
4.3. Results of the Experiment

To re-examine the proposed stator and rotor resistance estimation algorithms, an experimental setup has been developed (Figures 9 and 10). The experiment was performed on DS 1104 connected to the personal computer. Application of the controller is known in the literature for control of electronic converters, as in [39,40]. In this study, we use a three-phase induction motor 2.2 kW/400 V—detailed data are shown in Table 1. The motor is controlled by an inverter and is rigidly connected to a 1.5 kW dc motor—detailed data are shown in Table 2. The DC motor is controlled by a 4Q rectifier (Mentor II) in torque control mode (Torque Control) so that the load torque can be applied to the three-phase induction motor.

The current and flux controllers were implemented with a sampling time of 0.2 ms. The speed estimator using the sampling time is 2 ms, the rotor resistance estimation using the sampling time is 44 ms, the stator resistance estimation using the sampling time is 88 ms. An encoder with 5000 pulses/cycle was used to determine position and speed. The load torque is 2 Nm.

Table 2. DC motor parameters—Fuan LiYuan Electric, Ltd. (ZD97B-2).

| No | Parameters             | Values    |
|----|------------------------|-----------|
| 1  | Rated power            | 1.5 kW    |
| 2  | Rated frequency        | 50 Hz     |
| 3  | Rated armature voltage | 200 V     |
| 4  | Rated field voltage    | 200 V     |
| 5  | Rated field current    | 1.5 A     |
| 6  | Rated speed            | 1500 Rpm  |
In the low-speed region, the sensorless drive is more affected by the rotor and stator resistance estimation error than in the high-speed zone [9], so in this experiment, a low speed 20 rad/s is set as the reference speed value for the controller. After a number of tests, the learning rate to estimate rotor and stator resistance was chosen as follows: \( \eta_r = 0.015; \eta_s = 0.022 \). The motor runs for some time (around 60 min or more) with a load \( T_L = 2 \text{ Nm} \) (approximately 30% of the rated load). The obtained results are presented as follows:

- In Section 4.3.1, the comparison between estimation level with and without constant learning rate;
- In Section 4.3.2, the comparison between the speed of induction motor with and without online rotor and stator resistance estimators;
- In Section 4.3.3, the short discussion of obtained results is presented.

4.3.1. Results of Rotor and Stator Resistance Estimation

Figure 11a shows that the estimated rotor resistance with constant learning rate has an average value \( \approx 2.10 \Omega \). Figure 11b is an enlarged image of the rotor resistance estimation with constant learning rate, the estimated rotor resistance with constant learning rate, the pulsation of estimated
resistance ≈ 20%. The estimated rotor resistance using the learning rate by function (11) is almost non-pulsating, as indicated in Figure 11c. Figure 12a shows that the estimated stator resistance has an average value ≈ 2 Ω. In Figure 12b, the estimated stator resistance using the learning rate according to (18) is more accurate than using the constant learning rate (the pulsation of estimated stator resistance is ≈25% when the learning rate is constant, while with the proposed method, the pulsation of estimated stator resistance is ≈3%).

![Figure 11. (a) Estimated rotor resistance with learning rate is constant; (b) zoom of estimated rotor resistance with learning rate is constant; (c) estimated rotor resistance with learning rate as a function from Equation (11).](image1)

![Figure 12. (a) Estimated stator resistance with learning rate is constant; (b) estimated stator resistance with learning rate as a function from Equation (18).](image2)

4.3.2. Impact of Online Rotor and Stator Resistance Estimation

**Case study 1:** Without the online rotor and stator resistance estimation.

Figure 13a–d show that the measured speed is pulsating compared to the reference speed: the pulsation of measured speed is ≈5%; the estimated speed fluctuates around the reference speed; the pulsation of estimated speed is ≈6.25%.

**Case study 2:** With the online rotor and stator resistance estimation.

Figure 14a–d show that the measured speed is almost the same as the reference speed, and the pulsation is only ≈2%; the estimated speed also follows the reference speed, with the same pulsation of ≈2%.
4.3.2. Impact of Online Rotor and Stator Resistance Estimation

Case study 1: Without the online rotor and stator resistance estimation.

Figure 13. Speed of induction motor without online rotor and stator resistance estimation: (a,b) Reference speed and measurement speed; (c,d) Reference speed and estimated speed.

(a) 
(b) 
(c) 
(d)

Case study 2: With the online rotor and stator resistance estimation

Figure 14. Speed of induction motor with online rotor and stator resistance estimators: (a,b) Reference speed and measurement speed; (c,d) Reference speed and estimated speed.

(a) 
(b) 
(c) 
(d)

4.3.3. Discussion

The results presented in the previous section indicate that

- Estimated rotor resistance obtained from the proposed methodology ensures that the pulsation is 20% lower than with constant learning rate. Additionally, the level of pulsation of the proposed method is less than 1%, which is better than results obtained in, e.g., [16] (up to 5%);
• Estimated stator resistance obtained from the proposed methodology ensures that the pulsation is 22% lower than with constant learning rate. Additionally, the level of pulsation of the proposed method is less than 3%, which is better than results obtained in, e.g., [35] (not exceeding 10%); 

• Application of the proposed online rotor and stator resistance estimation ensured a decrease in the value of pulsation of over 4% than with constant learning rate.

The indicated results concern the quasi-steady operating state of the drive. Analysis of other operating states is an element for future research.

5. Conclusions

This paper proposes a method for estimating the rotor and stator resistance of an induction motor using artificial neural networks with the variable learning rate determined by a function. The results show that online rotor and stator resistance estimation using the proposed method is more accurate when estimating at a constant learning rate and also demonstrate that the online estimation of rotor and stator resistance has contributed to improving the control quality of the sensorless induction motor drive. Future direction of the research will be properties evaluation of the proposed method for various operating states.

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List of Symbols

| Symbol   | Description                                                                 |
|----------|-----------------------------------------------------------------------------|
| $\psi_{vmr}^\alpha$ | $\alpha$-axis rotor flux linkages estimated by voltage model in the stator reference frame |
| $\psi_{vmr}^\beta$ | $\beta$-axis rotor flux linkages estimated by voltage model in the stator reference frame |
| $\psi_{s}^\alpha$ | $\alpha$-axis stator flux linkages in the stator reference frame |
| $\psi_{s}^\beta$ | $\beta$-axis stator flux linkages in the stator reference frame |
| $\psi_{imr}^\alpha$ | $\alpha$-axis rotor flux linkages estimated by current model in the stator reference frame |
| $\psi_{imr}^\beta$ | $\beta$-axis rotor flux linkages estimated by current model in the stator reference frame |
| $V_{s}^\alpha$ | $\alpha$-axis stator voltage in the stator reference frame |
| $V_{s}^\beta$ | $\beta$-axis stator voltage in the stator reference frame |
| $i_{sa}$ | $\alpha$-axis stator current in the stator reference frame |
| $i_{sb}$ | $\beta$-axis stator current in the stator reference frame |
| $L_m$ | magnetizing inductance |
| $L_r$ | rotor self-inductance |
| $L_s$ | stator self-inductance |
| $R_s$ | stator resistance |
| $R_r$ | rotor resistance |
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