Kinetic Validation of the Models for P-Glycoprotein ATP Hydrolysis and Vanadate-Induced Trapping. Proposal for Additional Steps

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Abstract

P-Glycoprotein, a member of the ATP-binding cassette (ABC) superfamily, is a multidrug transporter responsible for cellular efflux of hundreds of structurally unrelated compounds, including natural products, many clinically used drugs and anticancer agents. Expression of P-glycoprotein has been linked to multidrug resistance in human cancers. ABC transporters are driven by ATP hydrolysis at their two cytoplasmic nucleotide-binding domains, which interact to form a closed ATP-bound sandwich dimer. Intimate knowledge of the catalytic cycle of these proteins is clearly essential for understanding their mechanism of action. P-Glycoprotein has been proposed to hydrolyse ATP by an alternating mechanism, for which there is substantial experimental evidence, including inhibition of catalytic activity by trapping of ortho-vanadate at one nucleotide-binding domain, and the observation of an asymmetric occluded state. Despite many studies of P-glycoprotein ATPase activity over the past 20 years, no comprehensive kinetic analysis has yet been carried out, and some puzzling features of its behaviour remain unexplained. In this work, we have built several progressively more complex kinetic models, and then carried out simulations and detailed analysis, to test the validity of the proposed reaction pathway employed by P-glycoprotein for ATP hydrolysis. To establish kinetic parameters for the catalytic cycle, we made use of the large amount of published data on ATP hydrolysis by hamster P-glycoprotein, both purified and in membrane vesicles. The proposed kinetic scheme(s) include a high affinity priming reaction for binding of the first ATP molecule, and an independent pathway for ADP binding outside the main catalytic cycle. They can reproduce to varying degrees the observed behavior of the protein’s ATPase activity and its inhibition by ortho-vanadate. The results provide new insights into the mode of action of P-glycoprotein, and some hypotheses about the nature of the occluded nucleotide-bound state.

Introduction

The multidrug transporter P-glycoprotein (Pgp, ABCB1) is a plasma membrane protein belonging to the ABC superfamily which couples the efflux of a wide variety of chemically and structurally different compounds to the hydrolysis of ATP [1]. Commonly used chemotherapy drugs are transported by Pgp, and its overexpression in tumour cells is linked to the multidrug resistant (MDR) phenotype that many human cancers present in the clinic [2,3]. Following the first report of Pgp ATPase activity [4], studies characterizing ATP hydrolysis were conducted in the early 1990s with plasma membrane preparations from MDR cell-lines [5], partially purified [6,7] or purified detergent-solubilized Pgp [8,9], and reconstituted Pgp [10,11]. Since then, the catalytic cycle of the enzyme, its coupling to drug transport, and its inhibition by ortho-vanadate (V_i) have been studied by several research groups [12,13].

In 1995, Senior’s group published a minimal reaction pathway for hydrolysis of one molecule of ATP by Pgp, and V_i-induced inhibition of its catalytic activity [14]. The protein possesses two consensus sequences for ATP binding, located within the two nucleotide binding domains (NBD1 and NBD2) in the highly homologous halves. In support of the proposed scheme for the catalytic reaction, it was demonstrated that both NBD1 and NBD2 are capable of binding and hydrolysing ATP [14–16]. Thus, the minimal reaction scheme presented for the hydrolysis of ATP and trapping by V_i corresponds to the catalytic activity carried out independently by each half-molecule. Consequently, the apparent single K_m observed for ATP hydrolysis [5,9], and the apparent single K_d reported for binding of nucleotides and nucleotide analogs observed by fluorescence and EPR spectroscopy [17–20], suggest that NBD1 and NBD2 are similar in their binding and kinetic properties in regard to the hydrolysis of ATP.

It is now generally accepted that the two NBDs of ABC proteins must interact to form a sandwich dimer for the normal functioning of these proteins, and such cooperativity has been shown for Pgp [21]. Thus, inactivation of one of the catalytic sites by either mutation [22] or chemical modification [15], or the formation of a non-covalent long-lived complex with V_i trapped at a single NBD [14,23], is enough to completely abolish the ATPase activity of the enzyme. As result, steady-state catalysis takes place only when both half-molecules are intact. In addition, stimulation of the basal ATP

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activity by drug substrates is displayed only when the full-length transporter is expressed, or both half-molecules are co-expressed [24].

Based on a minimal reaction scheme, Senior and co-workers [25] were the first to postulate a model for coupling between the catalytic activities of the two NBDs, under the name Alternating Catalytic Mechanism. In this model, the hydrolytic reactions of each half-cycle, and the accompanying protein conformational changes, alternate to carry out the transport of a drug molecule. The catalytic activity at NBD1 containing a bound ATP molecule is triggered when a second ATP molecule binds to NBD2, and vice versa. Thus, the reaction progresses in an alternating sequence of ATP binding and hydrolysis in the complementary half-molecules. In this model, the authors hypothesized that the transport of the drug is coupled to the relaxation of the protein from a high chemical potential state that is generated by the hydrolytic step. In one turnover of this cycle, two molecules of drug are transported and two molecules of ATP are consumed. This basic mechanism for the catalytic and transport cycle of the Pgp is currently widely accepted, with the addition of further adaptations based on structural and energetic considerations.

The Alternating Catalytic Mechanism suggests that asymmetry in the two halves of Pgp must be maintained throughout the catalytic cycle, in order to retain the memory of which NBD recently hydrolysed ATP [26]. Using Pgp carrying a mutation in an essential catalytic residue in both NBDs (E552A/E1197A), Tombline et al. demonstrated the existence of a stable asymmetric nucleotide-bound Pgp species [27]. After gel filtration chromatography the protein retained one molecule of ATP, which was bound (occluded) nucleotide-bound Pgp species [27]. After gel filtration chromatography the protein retained one molecule of ATP, which was bound (occluded) nucleotide-bound Pgp species [27]. The asymmetric species with a single tightly-bound ATP molecule was referred to as the occluded state. Sauna and co-workers reported the occlusion by wild-type Pgp of a single molecule of ATP/S, a very slowly hydrolysable nucleotide analog [28]. More recently, our laboratory reported the occlusion by wild-type Pgp of a single molecule of ATP/S, a very slowly hydrolysable nucleotide analog [28]. More recently, our laboratory reported the occlusion by wild-type Pgp of a single molecule of ATP/S, a very slowly hydrolysable nucleotide analog [28].

In spite of the great advances in understanding the ABC superfamily that have taken place over the last 15 years, no comprehensive kinetic analysis has been carried out to date. The compact mode of catalysis proposed by Senior’s group in 1995 has been used to establish possible transport mechanisms (e.g. it was used in the Sequential Mechanism proposed by Sauna and Ambudkar [30]), regardless of the fact that several puzzling experimental observations have only been described superficially, and no satisfactory explanation has yet been proposed for them. These previously ignored observations could possibly be key pieces of information in the development of a comprehensive kinetic model for the catalytic cycle of Pgp. In this work, we built several progressively more complex kinetic models, and then carried out simulations and detailed analysis to test their validity in the proposed reaction pathway for the Pgp-mediated hydrolysis of ATP and its inhibition by Vi. To establish kinetic parameters for the catalytic cycle, we made use of the large amount of accumulated data on verapamil-stimulated ATP hydrolysis by hamster Pgp, both purified and in membrane vesicles. We show that the proposed kinetic scheme(s), which include additional steps, can reproduce to varying degrees the observed behavior of the protein’s ATPase activity and its inhibition by Vi. The results provide new insights into the mode of action of Pgp, and some hypotheses about the nature of the occluded state.

Methods

Construction of the Elemental Cycle Kinetic Model

The basic kinetic cycle consists of an adaptation of the one originally proposed by Senior and co-workers in 1995 [14,25], here called the Elemental (Catalytic) Cycle (Figure 1). In it, a single reaction for binding and hydrolysis of MgATP is followed by sequential release of the products Pi and MgADP. For brevity, MgATP and MgADP will henceforth be referred to simply as ATP and ADP. Inhibition by Vi is achieved by formation of a long-lived complex, with ADP-Vi trapped in one catalytic site, by a single step. This complex is thought to resemble structurally the normal transition state conformation formed with Pgp. In our implementation, all the reaction steps were considered reversible except for the ATP hydrolytic step, which is irreversible [31].

The strategy used to test the validity of the reaction scheme in the Figure 1 consisted of the development of a kinetic model based on the rate law for each reaction. For modeling the scheme in the Elemental Cycle, the system was considered as a reaction medium without compartmentalization (which is the case for in vitro assays using solubilized enzyme or membrane vesicles) composed of the enzyme (E, Pgp) and one or more ligands (substrate, ATP; inhibitor, Vi; and products, ADP and Pi), for a total of n = 5 enzymatic intermediates. From the scheme in Figure 1, we formulated a set of ordinary differential equations for the rate of change of the concentration of n-1 intermediates; considering each reaction as an elementary mechanistic step. The reaction system was defined by a vector C_o of initial reactant concentrations, the total concentration of enzyme, [E]_o, and a vector k constituted of unimolecular and bimolecular rate constants, according to each unidirectional reaction, given by

$$k = \langle k_{1,1}, k_{2,2}, k_{3,3}, k_{4,4}, k_{5,5} \rangle$$

$$C_o = \langle [ATP]_o, [ADP]_o, [Pi]_o, [Vi]_o \rangle$$

with \([E]_0 < \langle [ATP]_o, [ADP]_o, [Pi]_o, [Vi]_o \rangle\). The two following biochemical variables were solved either symbolically or numerically:

![Figure 1](https://example.com/figure1.png)

**Figure 1. The Elemental Catalytic Cycle of Pgp and Vi-induced inhibition.** This scheme for the basic catalytic reaction for ATP hydrolysis by Pgp is adapted from Urbatsch et al. [14] E: Pgp. doi:10.1371/journal.pone.0098804.g001
(i) Turnover rate (in $s^{-1}$), $v$

$$ v = v(k, C_o, [E]) = \frac{k_s [E_{ATP}]}{[E]^1} | k, C_o $$

(ii) Fraction of trapped enzyme (adimensional), $T$

$$ T = T(k, C_o, [E]) = \frac{[E_{ADP,V}]_{1}}{[E]^1} | k, C_o $$

For modeling the other reaction schemes derived from the Elemental Cycle, in what are called extensions of the Alternating Cycle, additional differential equations were included to account for the new intermediates. In this regard, for the Partial-Extended Alternating Cycle (Figure 2, including blue reactions) the variables $v$ and $T$ are defined by the expressions

$$ v = v(k, C_o, [P]) = \frac{k_s [E_{ATP}]}{[P]^1} | k, C_o $$

$$ T = T(k, C_o, [P]) = \frac{[E_{ADP,V}]_{1} + [F_{ATP}]_{1}}{[P]^1} | k, C_o $$

with $P$, $E$ and $F$ defined in Figure 2, and the vector $k$ upgraded to include $\langle k_9, k_{-9} \rangle$. Furthermore, additional reaction paths were added to account for the Extended Alternating Cycle (Figure 2, including red reactions), for which the following new variables were defined: the fraction of single-nucleotide trapped species, $T_i$, and the fraction of two-nucleotide trapped species, $T_{II}$, given by

$$ T_i = T(k, C_o, [P]) = \frac{[E_{ADP,V}]_{1} + [F_{ATP}]_{1}}{[P]^1} | k, C_o $$

$$ T_{II}(k, C_o, [P]) = \frac{[E_{ADP,V}]_{1} + [F_{ATP}]_{1}}{[P]^1} | k, C_o $$

by upgrading the vector $k$ to include $\langle k_{14}, k_{15}, k_{a,} k_{a,} k_{a,} k_{a,} k_{a,} k_{a,} \rangle$.

The analytical solutions were obtained using the computational algebra package GROEBNER included in Maple 15 (MapleSoft Inc., Waterloo ON, Canada), while the general-purpose simulation package SCaP 3.5 (Simulation Resources Inc., MI, USA) was used for numerical integration. For some plotting and fitting procedures, OriginPro 8 was used (OriginLab Corp., MA, USA).

The solutions to these functions were used to kinetically evaluate the steady-state solutions of the biochemical variables for the Elemental Cycle correspond to the following expressions

$$ v_{SS} = \frac{k_{cat}[ATP]}{1 + \frac{[ADP]}{K_{aD}} + \frac{[ADP]}{K_{aD}}} + \left(1 + \frac{[P]}{K_{i}^P} + \frac{[P]}{K_{i}^P} \right) [ATP] $$

(1)

$$ T_{SS} = \frac{k_{cat}[ATP]}{1 + \frac{[ADP]}{K_{aD}} + \frac{[ADP]}{K_{aD}}} + \left(1 + \frac{[P]}{K_{i}^P} + \frac{[P]}{K_{i}^P} \right) [ATP] $$

(2)

with the steady-state concentration vector defined by $C_{SS} = \langle [ATP], [ADP], [P], [V] \rangle$. Eqs. 1–2 can be evaluated under the assumption that $C_{SS}$ is almost identical to $C_0$ under the experimental conditions, e.g. using low $[E]$, monitoring the initial rate of activity, and/or measuring the initial rate in the presence of an ATP-regenerating system. In both expressions, the thermodynamic parameters are defined by

(a) $K_{ATP} = k_{-1} k_1$ (b) $K_{P}^P = k_{-1} k_3$ (c) $K_{ADP}^P = k_{-4} k_4$ (d) $K_{V}^P = k_{-5} k_5$  (3)
Table 1. Phenomenological and thermodynamic parameters for the ATPase activity and Vi-induced trapping of Pgp.

| Parameter                          | Value       | System | [reactant] (mM) | [Ver] (μM) | Ref  |
|-----------------------------------|-------------|--------|----------------|------------|------|
|                                    |             |        | ATP            | ADP        | P_i  | V_i  |       |
| for ATP                           |             |        |                |            |      |      |       |
| \( k_{cat} \) for ATP             | 4.9 s\(^{-1}\) | P      | 0              | 9.2 s\(^{-1}\) | 0    | 50   | [8]   |
| \( K_d \) for ATP                 | 460 μM      | P\(^{ab}\) | 0              | 280 μM     | 0    | 0    | [20]  |
| \( K_m \) for ATP                 | 870 μM      | P\(^{ac}\) | 0              | 800 μM     | 0    | 50   | [8]   |
|                                    | 1500 μM     | PM     | 0              | 1200 μM    | 200  | 10   | [14]  |
|                                    | 1400 μM     | PM     | 10             | 330 μM     | 5    | 10   | [9]   |
|                                    | 300 μM      | P      | 10             | 0.9 μM      | 0.2  | 10   | [23]  |
| \( IC_{50} \) for trapping        | 9 μM        | PM     | 1.0            | 9 μM       | 1.0  | 0.2  | 10    | [23]  |
| % trapping                         | >90%        | PM     | 0.2            | >90%       | 1.0  | 0.2  | 10    | [23]  |
| \( t_{1/2} \) for trapping        | ~10 s       | PM     | 1.0            | 4.8 min    | 1.0  | 0.2  | 10    | [23]  |
| \( t_{1/2} \) for ATPase recovery | 84 min\(^{*}\)| PM     | ± 10.0        | 84 min\(^{*}\)| PM | ± 10.0 | [23] |
| for ADP                           |             | P\(^{b}\) |                |            |      |      |       |
| \( K_d \) for ADP                 | 330 μM      | P\(^{b}\) | 0              | 350 μM     | 0    | 10   | [5]   |
|                                    | 700 μM      | PM     | 50             | 700 μM     | 0    | 50   | [8]   |
| \( IC_{50} \) for trapping        | 15 μM       | PM     | 0.2            | 15 μM      | 1.0  | 0.2  | 10    | [23]  |
| % trapping                         | >90%        | PM     | 0.2            | >90%       | 1.0  | 0.2  | 10    | [23]  |
| \( t_{1/2} \) for trapping        | 4.8 min     | PM     | 1.0            | 4.8 min    | 1.0  | 0.2  | 10    | [23]  |
| \( t_{1/2} \) for ATPase recovery | 84 min\(^{*}\)| PM     | ± 10.0        | 84 min\(^{*}\)| PM | ± 10.0 | [23] |
| for P\(_i\)                       |             | PM     |                |            |      |      |       |
| \( IC_{50} \) for hydrolysis      | 200 mM      | PM     | 1.0            | 200 mM     | 1.0  | 10   | [14]  |
| % trapping                         | >90%        | PM     | 0.2            | >90%       | 0.2  | 0.2  | 10    | [14]  |
| \( t_{1/2} \) for trapping        | 70 mM       | PM     | 0.2            | 70 mM      | 1.0  | 0.2  | 10    | [23]  |
| % trapping                         | 85%         | PM     | 0.2            | 85%        | 1.0  | 0.2  | 10    | [23]  |
| \( t_{1/2} \) for trapping        | 81%         | PM     | 0.2            | 81%        | 1.0  | 0.2  | 10    | [23]  |
| for V\(_i\)                       |             | PM\(^{f}\) |                |            |      |      |       |
| \( IC_{50} \) for hydrolysis/trapping | 12 μM   | PM\(^{f}\) | 2.5          | 12 μM     | 1.0  | 10   | [5]   |

Kinetic Models for P-Glycoprotein ATP Hydrolysis
and the kinetic parameters by

\[ \frac{k_{cat}}{k_d} = h_2^2 \]  
\[ k_m = \frac{1}{3} \left( K_{ATP}^P + K_{ATP}^P \right) \]
\[ K_{ATP}^P = \beta \cdot K_d^P \]
\[ K_d^P = \beta \cdot K_d^P \]

(4)

where the factors \( \alpha \) and \( \varphi \) are defined as

\[ \alpha = \frac{k_{-4}}{k_2} \]
\[ \varphi = k_2 \left( 1 + \frac{1}{k_{-3}} + \frac{1}{k_{-4}} \right) \]

(5)

From these basic parameters we derived the phenomenological parameters, \( K_{ATP}^P \) and \( IC_{50} \), for the observed steady-state turnover rate and trapped fraction. However, in the absence of rapid kinetic data for Pgp-mediated ATP hydrolysis, it was necessary to use an arbitrary setting for the vector \( k \). Although, the exact values of the vector \( k \) are unknown, the settings specified here were designed to reproduce as closely as possible the published experimental data in Table 1. The rationalization of the Elemental Cycle rate constants is as follows:

(i) The observed catalytic rate, \( k_{cat} \approx 10^4 \text{s}^{-1} \) is equivalent to \( \nu_{max} \approx 10 \mu \text{mol Pgp} \cdot \text{mg}^{-1} \cdot \text{min}^{-1} \) [8]. Since two ATP are hydrolyzed per Pgp in the full catalytic cycle (see Alternating Cycle below) the rate constant for the hydrolytic step was set to \( k_2 = 20 \text{s}^{-1} \) (Eq. 4a).

(ii) In the absence of products and inhibitors, Eq. 1 presents the characteristic hyperbolic behavior observed for the ATP dependence of ATP hydrolysis by Pgp, according to

\[ \nu_{SS} = \frac{k_{cat} [ATP]}{K_m + [ATP]} \text{ when } [\text{ADP}] = [P] = [V_i] = 0 \]

(6)

with parameters within the range reported: a maximal turnover rate of \( k_{cat} \), and a high consensus Michaelis-Menten constant of \( K_m \approx 588 \mu \text{M} \) for verapamil-stimulated Pgp [5,8]. The low affinity of ATP was set at \( K_{ATP}^P = 1000 \mu \text{M} \), based on a reference value of \( 1 \text{ mM} \) for the effect of ATP on inhibition of labeling of NBD1 by 8-azido-ATP [16]. From the selected \( K_m \) and \( K_{ATP}^P \) values, and \( \varphi \approx 2 \), the ratio \( k_2/k_1 \) is predicted to be high (~200, Eq. 4b), from which the rate constant for the association of ATP is estimated to be \( k_1 = 0.1 \mu \text{M}^{-1} \text{s}^{-1} \).

(iv) ADP was reported to compete with ATP for the nucleotide-binding site [5,9]. Effectively, the mathematical model predicts pure competitive inhibition behavior of ADP on ATP hydrolysis (Figure S1) according to

\[ \nu_{SS} = \frac{k_{cat} [ATP]}{K_m \left( 1 + \frac{[\text{ADP}]}{K_d} \right) + [ATP]} \text{ when } [\text{P}] = [V_i] = 0 \]

(7)
with $K_{\text{app}}$ increasing with ADP concentration. Eq. 7 states that the ADP inhibition constant for ATP hydrolysis, $K_{\text{ADP}}^{i}$, indeed corresponds to the ADP affinity, $K_{\text{ADP}}^{d}$. Thus, for a given $K_m$, the ADP affinity is constrained by the observed $K_{\text{app}}$. Herein, $K_{\text{ADP}}^{d}$ was set at 500 μM, which is compatible with the experimental value. (v) Given $K_{\text{Pi}}^{i} = 204$ mM, which is close to the reported value [14], Figure 3 shows the simulated output of the hydrolytic activity when [ATP] and [Pi] were varied, according to

$$v_{\text{SS}} = \frac{k_{\text{cat}}[\text{ATP}]}{1 + \frac{[\text{Pi}]}{K_{\text{Pi}}^{i}}}$$

when [ADP] = [V_i] = 0 \hspace{1cm} (8)

$K_{\text{Pi}}^{i}$ constrains the value of the affinity constant for binding of Pi to the complex $E_{\text{ADP}}$. Thus, given the value of φ and $\alpha = 1$ (i.e. $k_{-4} = k_2$), $K_{\text{Pi}}^{i}$ is estimated to be 100 mM (Eq. 4c). (vi) Inhibition of ATPase activity following reaction with $V_i$ has been extensively studied. It was demonstrated early on that the trapped species is the long-lived $\text{Pgp} \rightarrow \text{ADP} \rightarrow V_i$ complex, independent of the nucleotide used, and that the release of ADP correlates well with the slow reactivation of the enzyme [23]. The initial rate of ATPase activity, measured after rapid (~30 s) removal of unbound ligands, is approximately proportional to the relative concentration of untrapped enzyme. From Eq. 1, the ATP dependence of $V_i$ inhibition is described by

$$v_{\text{SS}} = \frac{k_{\text{cat}}[\text{ATP}]}{1 + \frac{[V_i]}{K_{V_i}^{i}}}$$

when [ADP] = [Pi] = 0 \hspace{1cm} (9)

According to Eq. 9, $IC_{50}^{V_i}$ corresponds to the solution of the following equation for $[V_i]$. (vii) Table 2. Rate constants for the Elemental Catalytic Cycle.

| Process               | Parameter | $K_d$     | $k$       |
|-----------------------|-----------|-----------|-----------|
| ATP association       | $k_1$     | $0.1 \text{ μM}^{-1}\text{s}^{-1}$ |           |
| ATP dissociation      | $k_{-1}$  | 100 s$^{-1}$ |           |
| ATP hydrolysis        | $k_2$     | 20 s$^{-1}$ |           |
| Pi association        | $k_3$     | 5 mM$^{-1}$s$^{-1}$ |           |
| Pi dissociation       | $k_{-3}$  | 500 s$^{-1}$ |           |
| ADP association       | $k_4$     | 0.04 μM$^{-1}$s$^{-1}$ |           |
| ADP dissociation      | $k_{-4}$  | 20 s$^{-1}$ |           |
| V association         | $k_5$     | 0.015 μM$^{-1}$s$^{-1}$ |           |
| V dissociation        | $k_{-5}$  | 0.020 s$^{-1}$ |           |
| $K_{\text{ATP}}^{d}$ | 1000 μM   |           |           |
| $K_{\text{Pi}}^{d}$  | 100 mM    |           |           |
| $K_{\text{ADP}}^{d}$ | 500 μM    |           |           |
| $K_{\text{Vi}}^{d}$  | 1.3 μM    |           |           |

Rate constants defining the vector $k$ for the reaction scheme shown in Figure 1. The nomenclature of the subscripts is follows: (± 1) for the ATP equilibrium, (± 2) for the hydrolytic step, (± 3) for the Pi equilibrium, and (± 4) for the ADP equilibrium. A positive sign is used for association reactions, a negative sign for dissociation reactions. doi:10.1371/journal.pone.0098804.t002

Table 3. Rate constants for the priming reaction of the PE Alternating Cycle.

| Process               | Parameter | $K_d$     | $k$       |
|-----------------------|-----------|-----------|-----------|
| ATP association       | $k_0$     | 10 μM$^{-1}$s$^{-1}$ |           |
| ATP dissociation      | $k_{-0}$  | 50 s$^{-1}$ |           |
| $K_{\text{ATP}}^{d}$ | 5 μM      |           |           |

Rate constants defining the vector $k$ in conjunction with the rates in Table 2, for the blue reactions in Figure 2. The nomenclature of the subscripts is as follows: (± 0) for the ATP priming equilibrium. doi:10.1371/journal.pone.0098804.t003

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Table 4. Complementary rate constants for the Extended Alternating Cycle.

| Process          | Parameter | \( K_a \)  | \( k \)  |
|------------------|-----------|------------|--------|
| ADP association  | \( k_{aA} \) | 0.04 \( \mu M^{-1}s^{-1} \) |        |
| ADP dissociation | \( k_{dA} \) | 2 s^{-1} |        |
|                  | \( K_{ADP} \) | 50 \( \mu M \) |        |
| ATp association  | \( k_{A} \) | 2 \( \times \) 10^{-5} \( \mu M^{-1}s^{-1} \) |        |
| ATp dissociation | \( k_{dA} \) | 1 \( \times \) 10^{-4} s^{-1} |        |
|                  | \( K_{ATP} \) | 5 \( \mu M \) |        |
| ATp dissociation | \( k_{dA} \) | 1 \( \times \) 10^{-5} \( \mu M^{-1}s^{-1} \) |        |
|                  | \( K_{ATP} \) | 30 mM |        |

Rate constants defining the vector \( \mathbf{k} \) in conjunction with the rates in Table 2 and Table 3, for the red reactions in Figure 2. The nomenclature of the subscripts is the same as in Table 2, with the addition of the suffix \( a \) to identify this pathway.

\[ \frac{k_{cat}}{(1+[Pi]/K_{iPi})} \frac{[ATP]}{[ATP]} = \frac{1}{2} \frac{k_{cart}[ATP]}{K_m+[ATP]} \]  \hspace{1cm} (10a)

resulting in

\[ IC_{ATP}^{Vi} = [Vi] \frac{[ATP]}{2M_{ATP}([Pi]=0)} = K_{Vi}^{Vi} \left( \frac{K_m}{[ATP]} + 1 \right) \]  \hspace{1cm} (10b)

which is the same as \( K_{Vi}^{Vi} \) for the \( Vi \) concentration dependence of ATP hydrolysis. Setting \( K_{Vi}^{Vi} = 1.33 \mu M \), yields \( K_{Vi}^{Vi} = 2.72 \mu M \) (Eq. 4d) and the \( IC_{ATP}^{Vi} \) corresponds to 4.32 \( \mu M \) at 1 mM ATP (see Figure 4A). A value close to 4.0 \( \mu M \) was reported for half-maximal inhibition of Pgp ATPase activity by \( Vi \) under the same conditions [23]. Similarly, the trapped fraction variable was a query in our analysis. The steady-state concentration of trapped enzyme defined in Eq. 2 follows a hyperbolic curve as the ATP concentration increases, according to

\[ T_{SS} = \frac{[ATP]}{K_m + [ATP]} \times \frac{[ATP]}{k_{cat}} \times \frac{1}{K_{iPi}^{Vi} + [Pi]} \]  \hspace{1cm} (11)

At saturating \( Vi \) concentration (e.g. 200 \( \mu M \)), the \( IC_{ATP}^{Vi} \) is indeed the “\( K_{ATP}^{app} \)” term in Eq. 11, which for the given \( K_{Vi}^{Vi} \) value yields \( IC_{ATP}^{Vi} \approx 7.9 \mu M \), close to the reported value of 9.0 \( \mu M \) [23] (see Figure 4B for the untrapped fraction). (vii) Given the value of \( k_{dA} \) and \( K_{ADP} = 500 \mu M \), \( k_{dA} \) was estimated to be 0.04 \( \mu M^{-1}s^{-1} \) [Eq. 3c]. This does not agree with \( k_{dA} = 1.2 \times 10^{-5} \mu M^{-1}s^{-1} \) as suggested by Urbatsch et al. [23] based on the kinetics observed for ADP trapping following the route \( E \xrightarrow{k_{dADP}} [ATP] \xrightarrow{k_{Vi}} EADP \xrightarrow{k_{Vi}} Vi \) [23]. Thus, for the given \( k_1 \) (and \( k_{-1} \) and \( k_2 \), reaction with \( Vi \) becomes the

Figure 3. Effect of \( Pi \) on Pgp ATPase activity. Semi-log plot from the evaluation of \( \frac{\text{Turnover rate}}{[ATP]} \times 10^3 \) with \( C_{ATP} = ([ATP]_0,[Pi]_0) \) for \( [Pi]_0 = 0 \) (red), 50 \( mM \) (green), 200 \( mM \) (yellow) and 1000 \( mM \) (blue). Inset: double-reciprocal plot with ATP concentrations ranging upwards from 100 \( \mu M \). Values of \( \mathbf{k} \) are given in Table 2.

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rate-limiting step, with a calculated lower limit of about 0.0015 μM⁻¹s⁻¹. However, taking into account the other pathway for breakdown of the intermediate \(E^{ADP}\) in the absence of \(P_i( E^{ADP} \xrightarrow{k_{-4}} E, \text{with } k_{-4} = 20 \text{ s}^{-1})\), \(k_4\) was here set to 0.015 μM⁻¹s⁻¹.

Table 2 presents the assigned values of the rate constants (using
the arguments above) for the 9 unidirectional reactions defining
the vector \(k\), and the derived dissociation constants, \(K_i\) for the 4
bidirectional steps (Eq. 3). Once defined, \(k\) was kept constant
for the rest of the simulations and validations.

The effect of \(P_i\) on ATPase activity was a key element in the
validation of the model. It was previously reported that \(P_i\) behaves
as a mixed-type inhibitor of ATP hydrolysis [23], where 200 mM
\(P_i\) reduces the apparent \(v_{max}\) by 50%, while the apparent \(K_m\) is
reduced by just 20% [14]. In contrast, according to Eq. 8, \(K_{app}^{ADP}/
K_m^{ADP}\) (the slope of the lines in the Lineweaver-Burk plot, see
Figure 3 inset) is independent of inhibitor concentration, since
\(K_{cat}^{ADP}/K_m^{ADP} = K_{cat}/K_m\), so that \(P_i\) behaves instead as an uncom-
petitive inhibitor, which is incongruent with the reported data.

Another inconsistency between the output of the model and
experimental data comes from trapping with ADP. It has been
reported that 15 μM ADP produces half-maximal inhibition in the
presence of 200 μM \(Vi\) [23]. According to Eq. 2, the ADP
dependence of the trapping is defined by

\[
T_{SS} = \frac{\left(\frac{[Vi]}{K_d^{ADP}+[Vi]}\right)[ADP]}{K_d^{ADP} + \left(1 + \frac{[Vi]}{K_d^{ADP}}\right)[ADP]} \quad \text{when } [ATP] = [P_i] = 0 \tag{12}
\]

where at saturating \(Vi\), the “\(K_d^{ADP}\) term corresponds to \(IC_{50}^{ADP}\) (as
with ATP dependence, see Eq. 11). Thus at 200 mM \(Vi\), given the
\(K_d^{ADP}\) and \(K_d^{Vi}\) values, the calculated \(IC_{50}^{ADP}\) is 3.31 μM, which is
5-fold lower than the reported value [23].

Figure 4B presents the simulated nucleotide dependence of the
untrapped (free) fraction, \(1-T_{SS}\), for both cases given by the model in
Figure 1. Fitting of the synthetic data gave a Hill number of
\(n = 1\) for both ATP and ADP, which is expected for binding of just
one nucleotide according to Eqs. 11 and 12. However, the behavior reported experimentally was a steeper concentration
dependence for both ATP and ADP [23].

The ability of \(P_i\) to protect Pgp from \(Vi\) trapping was also tested
using the model. It was reported that in the presence of 200 μM
\(Vi\), protection by 200 mM \(P_i\) is negligible at 1 mM ATP, but
becomes significant at lower ATP concentrations [23]. This
differential \(P_i\) protection effect depending on ATP concentration
could not be reproduced by the model in Figure 1. The evaluation of \(T_{SS}\)
as a function of [ATP] and \(P_i\), in the presence of 100 μM \(Vi\) is plotted in
Figure 5, which shows lines of similar slope, and ATP dependence opposite to that observed experimentally, i.e. the slopes decrease at lower ATP concentration.

From Eq. 2, \(K_{d,app}^{Vi}\) decreases with increasing [ATP] according to

\[
K_{d,app}^{Vi} = K_d^{Vi}\left(1 + \frac{[Vi]}{K_m^{ATP}}\right) \quad \text{when } [ADP] = 0 \tag{13}
\]
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\[
K'_{V_i}^{app} = K'_{V_i} \left(1 + \frac{K_m}{[ATP]} + \frac{[P_i]}{K'_{Vi}}\right) \text{ when } [ADP] = 0 \tag{14a}
\]

\[
K'_{d}^{app} = K'_{d} \left(1 + \frac{K'_{ADP}}{[ADP]} + \frac{[P_i]}{K'_{dVi}}\right) \text{ when } [ADP] = 0 \tag{14b}
\]

However, fitting of the synthetic data in Figure 6 to an expression using an effective inhibition constant for \(P_i\), \(K'_{effVi}\), according to

\[
K'_{V_i}^{app} = K'_{V_i} \left(1 + \frac{[P_i]}{K'_{Vi}}\right) \text{ when } [ADP] = 0 \tag{15a}
\]

\[
K'_{d}^{app} = K'_{d} \left(1 + \frac{[P_i]}{K'_{dVi}}\right) \text{ when } [ADP] = 0 \tag{15b}
\]

yields values of \(K'_{effVi} = 51.8\) and \(45.4\) mM, for trapping with 200 μM of ATP and ADP, respectively, half the reported values of 100 and 70 mM, respectively, after correction for ionic strength [14]. The experimental values might be matched by increasing \(K'_{Vi}\), but then the capacity of \(P_i\) to inhibit hydrolytic activity would be affected (see [14]).

Considering the time domain, Figure 7A shows the time-course of the overall activity and formation of the trapped species, for a pulse of ATP and \(V_i\). Thus, evaluating \(T\) with 200 μM \([ATP]\) and \([P_i]\) (keeping both constant), the numerical simulation mimics the rapid formation of the trapped species (within 10 s) and the high steady-state fraction trapped that was reported in the literature [23]. However, the output of the model clearly disagrees with the reported transient kinetics of dissociation of the \(V_i\)-trapped state. Experimentally, upon removal of unbound ligands, the observed slow dissociation has \(k_{obs} = 1.4 \times 10^{-4} \text{ s}^{-1}\) (\(t_{1/2} = 87\) min) [23], which correlates with the recovery of ATPase activity by the pathway (Figure 1). The step \(E^{ADP} \rightarrow E\) occurs at the rate of \(k_{-4} = 20\text{s}^{-1}\), which is compatible with the turnover rate, and rules out this reaction as the rate-limiting step for recovery of activity. On the other hand, the step \(E^{ADP} \rightarrow E^{ADP} V_i\) with \(k_{-5}\) has a rate constant \(k_{-5} = k_{4} \cdot K'_{Vi} = 0.02\text{s}^{-1}\), which is 140-fold higher than the observed dissociation rate. Thus, in order to match the observed kinetics of ATPase recovery either (i) the dissociation constant \(K'_{Vi}\) must be much lower than 0.01 μM (see Figure 7B), a value which is incompatible with the observed \(K'_{Vi}\) for trapping with ADP and ATP (see above), or (ii) the association constant \(k_{5}\) must be much lower than 0.015 s⁻¹, which is incompatible with the fast formation of the trapped species (Figure 7A).

The slow recovery of ATPase activity from the trapped species might be explained by the existence of several hidden transitions in the overall reaction \(E^{ADP} \rightleftharpoons V_i \rightarrow E^{ADP} V_i\). This possibility was tested by adding a step with a low dissociation rate constant (< 0.001 s⁻¹) to explain the slow backward reaction to form \(E^{ADP}\). Effectively, the pathway for the trapping reaction was substituted by \(E^{ADP} \rightleftharpoons V_i \rightarrow E^{ADP} V_i\), which describes consecutive equilibria with \(K'_{Vi}\) and \(K'_{dVi}\), dissociation constants, respectively. In order to include a slow backward step and shift the equilibrium toward the species on the right, the new forward rate constant \(k_{6}\) was set to \(1 \times 10^{-7} \text{ s}^{-1}\) and the backward rate constant \(k_{-6}\) to \(1 \times 10^{-4} \text{ s}^{-1}\) (yielding \(K'_{dVi} = 0.1\)), with a concordant increase of the \(V_i\) association equilibrium constant \(K'_{Vi}\) to \(~10\times K'_{Vi}\). In this way, it would be possible to explain the slow recovery of ATPase activity, while the change in overall affinity of \(V_i\), \(K'_{Vi}\), would not significantly affect the \(K'_{Vi}\) for trapping with ADP and ATP. However, inclusion of this additional step could still not explain the slow inhibition observed with ADP, by the pathway \(E \rightarrow E^{ADP} \rightarrow E^{ADP} V_i\). This issue will be considered further below.

Construction of the Alternating Catalytic Cycles

In this section, we evaluate the Alternating Catalytic Cycle proposed by Senior et al. [25]. In our adaptation of the model (shaded cycle, Figure 2), the two equivalent forms of the enzyme, \(E\) and \(F\), correspond to states of the enzyme with similar energetic and/or conformational states that differ only in the hydrolytic properties of their individual NBDs. This notation is necessary to distinguish between the two-nucleotide species, \(E_{ATP} \neq F_{ATP}\), according to their NBD hydrolytic activity, i.e. the \(F\)-form is capable of hydrolyzing only the ATP molecule bound at NBD1 (but not at NBD2), and vice versa for the \(E\)-form, thus moving the enzyme symmetrically between both states. Two different models can account for the \(E/F\) forms; in both it is necessary to include ATP binding at each NBD of the bare enzyme as a first step (priming reaction) to get the initial intermediates of the cycle: (i) starting from the same conformer of the enzyme, \(P\), recruitment of the NBDs to the nucleotide-bound state occurs randomly, with the

![Figure 5. Protection of Pgp from \(V_i\) trapping by \(P_i\). Plot of the \(P_i\) concentration dependence of the trapped enzyme fraction with 100 μM \(V_i\) and different ATP concentrations, from the evaluation of \(T_{\text{ss,ki}}\), with \(C_{\text{ss}} = (\{ATP\},0,[P_i]),100\) for \([ATP]=1000 \mu M\) (red), 200 (green), 100 (yellow) and 20 μM (blue). Values of \(k_i\) are given in Table 2. doi:10.1371/journal.pone.0098804.g005](https://www.plosone.org)
probability of occupancy given by the intrinsic affinities of each NBD, so that 

\[ P_{\text{ATP}} \]  

or 

\[ P_{\text{ADP-P}} \]  

where binding takes place at NBD1, or 

\[ P_{\text{FATP}} \]  

where binding take place at NBD2), or (ii) both conformers of the empty protein (E and F) co-exist, each exhibiting its own constitutive binding properties (E allows binding at NBD1, while F allows binding at NBD2); they may or may not be kinetically connected by the equilibrium E \( \leftrightarrow \) F. The kinetics of ATP hydrolysis and Vi trapping are identical in both models. For the sake of simplicity, we decided to work with the first model, with the conservation of mass given by

\[
[P]_t = [P] + \sum_{ij} \left( [E_i] + [F_j] \right)
\]

with \( i,j \) for: none, ATP, ADP, ADP-P, and ADP-Vi, according to Figure 2. In this model, the intermediates \( E^{\text{ATP}} \) and \( F^{\text{ATP}} \) exhibit the same properties regardless of their origin, whether from the priming reaction or a later hydrolytic event. In this particular implementation of the Alternating Cycle, transformation between the two forms was achieved by exchange of ADP from/to the two-nucleotide intermediates to/from the one-nucleotide intermediates: \( E^{\text{ADP}} \leftrightarrow F^{\text{ADP}} \) and \( F^{\text{ATP}} \leftrightarrow E^{\text{ATP}} \), respectively. However, it would be equivalent to assign the transformation to either the hydrolytic step (which looks reasonable) or the P,

Figure 6. Effect of P, on the Vi dependence of trapping. Semi-log plot of the Vi concentration dependence of the untrapped enzyme fraction incubated with (A) 1000 μM ATP or (B) 1000 μM ADP, from the evaluation of \( T_{\text{SS}} \) with \( C_{\text{SS}} = \langle 1000,0,[P],[Vi] \rangle \) and \( C_{\text{SS}} = \langle 0,1000,[P],[Vi] \rangle \), respectively, for \( [P]_o = 0 \) (red), 200 μM (green), and 1000 μM (yellow). Values of k are given in Table 2.

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Figure 7. Time-course of ATPase activity and formation of trapped Pgp. (A) Transient behavior of ATPase activity (red) and the fraction of trapped enzyme (blue), evaluating \( T_{\text{KC}} \) with \( C_{\text{SS}} = \langle [ATP]_p,0,0,[Vi] \rangle \) at the indicated concentration pulses of ATP and Vi. (B) Time-course of the fraction of trapped Pgp according to Vi affinity. Transient behavior of the fraction of trapped enzyme on incubation with ATP and Vi, evaluating \( T_{\text{KC}} \) with \( C_{\text{SS}} = \langle [ATP]_p,0,0,[Vi] \rangle \) for pulses of 200 μM ATP and Vi of 50 s duration (not shown). Each curve corresponds to \( K_{\text{Vi}} = 3 \) μM (blue), 0.1 μM (black) and 0.01 μM (red). Values of k are given in Table 2; \( [P]_t = 0.25 \) μM.

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dissociation step, since in either case, the kinetic behavior of the system is the same. To maintain symmetry, this step was assigned to the dissociation/association of ADP, which is the last hydrolysis product to leave the NBD. In addition, it was necessary to include the trapping reactions with $V_i$ for each half-cycle ($E_{ATP} \leftrightarrow E_{ADP}^{Vi}$ and $F_{ATP} \leftrightarrow F_{ADP}^{Vi}$).

It is remarkable that neither of these two obvious steps (the priming and trapping reactions) has been depicted explicitly in any reaction scheme that considers both half-cycles simultaneously. The former was added later for first time by Urbatsch et al. [32], who considered that both NBDs binds ATP independently (priming reaction) and then come together (dimerization) to form the species with two bound ATP (although their concept was different from the one proposed here, see Discussion). We describe this new kinetic model, with both priming and trapping reactions (grey cycle plus blue reactions in Figure 2), as the Partial-Extended (PE) Alternating (Catalytic) Cycle. Any differences between the properties of the PE Alternating Cycle and a tandem repeat of the Elemental Cycle, can arise only from these additional reactions steps. Therefore, we were interested in evaluating the influence of the priming reactions in the ATP dependence of several observables. The steady-state solutions of the biochemical variables for the PE Alternating Cycle correspond to the following expressions

$$v_{SS} = \frac{k_{cat}[ATP]^2}{K_{ATP}^2 + [ATP]}$$

(16)

$$T_{SS} = \frac{k_m}{k_{cat}[ATP]^2 + [ATP]}$$

(17)

with the steady-state concentration vector defined by $C_{SS} = \{[ATP],[ADP],[Pi],[Vi]\}$. For the evaluation of Eqs. 16 and 17, it was assumed that $C_{SS} \cong C_0$, as explained earlier. For this model, the velocity and trapping equations are no longer hyperbolic. For example, the ATP dependence of the turnover rate now follows a quadratic equation given by

$$v_{SS} = \frac{k_{cat}[ATP]^2}{K_{ATP}^2 + [ATP]}$$

(18)

where $k_{cat}$ and $K_m$ are the parameters corresponding to the previous model (the Elemental Cycle), and the ATP affinity of the bare enzyme is defined by $K_{ATP}^0 = k_{cat}/k_0$. It is important to note that, whatever the relative value of $K_{ATP}^0$, Eq. 18 can be adequately fitted to the function

$$v_{SS} = \frac{k_{cat}[ATP]^n}{K_m + [ATP]^n}$$

when $[ADP] = [Pi] = [Vi] = 0$

(19)

with $n \geq 1$ and $K_m$ being an effective Michaelis-Menten constant. It is interesting to note that if $K_{ATP}^0 \cong K_{ATP}$, the deviation from hyperbolic is appreciable only at high ATP concentrations. On the other hand, if we consider a much lower $K_{ATP}^0 (< K_{ATP})$, $n$ approaches 1 and the deviation from hyperbolic is negligible, and only observed at very low ATP concentrations. Because the majority of reports describe Pgp ATPase activity as Michaelian, we set the value of $K_{ATP}^0$ in the μM range. This value also matched the low $K_m$ value for the poorly-hydrolysable analog ATPS [29] and other experimental evidence [33] explained by the model (see Discussion). Thus, simulating the PE Alternating Cycle with the parameters in Tables 2 and 3, the fitting that describes the ATP dependence of activity is an effective single $K_m$ of 596 μM for $n = 1$, a value very close to that obtained for the Elemental Cycle (Figure 8A).

The interaction with ADP is now no longer one of simple competition (Figure 8B), and is described by

$$v_{SS} = \frac{k_{cat}[ATP]^2}{K_{ATP}^0 + [ATP]^2}$$

(20)

when $[Pi] = [Vi] = 0$

unless we include a pathway for the reaction $P \rightarrow ADP$ and its equivalent for the $F$-form (shown in Figure 2 in red, but not considered at this stage). Nevertheless, at high ATP concentration (e.g. [ATP] > 100 μM, the behavior is apparently competitive, as the literature indicates (Figure 8B), since the interaction occurs mainly inside the catalytic cycle (where both nucleotides compete for the vacant site in $E_{ATP}$ and $F_{ATP}$), and the concentration of the bare enzyme, $P$, is negligible at that ATP concentration (see Figure 9).

As expected, the observed properties with respect to $P_i$ remained constant, with an effective inhibition constant, $K_{PI}$, of ~200 mM, since the relationship between the phosphate binding step and the hydrolytic step is conserved between the Elemental Cycle (or tandem repeats of it) and the PE Alternating Cycle. However, the double-reciprocal plot of the ATP dependence of activity (not shown) has an upward curvature given by

$$\frac{1}{v_{SS}} = \left(1 + \frac{K_{ATP}^{PI}}{K_{ATP}^{0}}\right) + \frac{k_m}{k_{cat}[ATP]} + \frac{1 + [Pi]}{k_{cat}K_{PI}^T}$$

(21)

when $[ADP] = [Pi] = 0$

revealing that indeed the slopes are $P_i$-independent (as for the Elemental Cycle), but are now affected by the ATP concentration.

$V_i$ also behaves similarly in the PE Alternating Cycle, inhibiting ATPase activity at low concentrations. As indicated previously, the Alternating Cycle by itself cannot explain the cooperativity found in the nucleotide dependence of $V_i$ trapping. This cooperative behaviour arises because of the priming reaction in the PE Alternating Cycle. From Eq. 17, producing synthetic data for the untrapped fraction, $1-T_{SS}$, with parameter values of $K_{ATP}^{0} = 5 \mu$M and $K_{PI}^T = 1.33 \mu$M (Figure 10), and performing an unweighted fitting according to

$$1 - T_{SS} = \frac{[ATP]^n}{K_{ATP}^{0} + [ATP]^n}$$

when $[ADP] = [Pi] = 0$

(22)
For the priming binding reaction with ATP, $P \overset{b_{1}[ATP]}{\rightarrow} E_{ATP}$ or $E_{ATP}$, the association rate constant was set to 100-fold the value for the corresponding rate inside the cycle, $E_{ATP} \overset{b_{1}[ATP]}{\rightarrow} E_{ATP}$ (and the $F$-form equivalent), which is $k_0 \approx 10 \text{ M}^{-1}\text{s}^{-1}$. Thus, the priming reaction would not limit the establishment of steady-state catalysis. In addition, this relatively high value for the priming association rate constant permits further decreases to allow our model to explain the observed impairment in trapping behavior in some systems [29,34].

However, some important experimental data still remain unexplained according to the PE Alternating Cycle: (i) the slow kinetics of $V_i$ inhibition with ADP, (ii) the slow kinetics of reactivation of ATPase activity, and (iii) the stoichiometry of 1:1 P-gp:nucleotide in the trapped species, where ADP is trapped with $V_i$. Indeed, according to the kinetic reactions in the PE Alternating Cycle (Figure 2, grey cycle plus blue reactions only), the trapped species should contain both ATP and ADP ($E_{ATP}$) and $E_{ATP,V_i}$, since there is no direct pathway to release ATP before $V_i$ release. Furthermore, according to this scheme, the bound ATP would be hydrolyzed when the enzyme re-enters the cycle upon $V_i$ release.

As pointed out above, there is the need to add plausible steps that account for the observed kinetics of trapping and release of both nucleotides. If we now incorporate the red reactions, Figure 2 outlines a minimal reaction pathway, including (i)

### Table 2

| Species | Reaction | Rate Constant |
|---------|----------|---------------|
| $E_{ATP}$ | $k_{1}$ | $k_{1}$ |
| $E_{ATP}$ | $k_{-1}$ | $k_{-1}$ |
| $P$ | $k_{p}$ | $k_{p}$ |
| $E_{ATP}$ | $k_{s}$ | $k_{s}$ |

We obtained a Hill number of $n = 1.21$ and $k_{v,app}$ or $IC_{SS}^{ATP}$ of $\approx 20 \mu M$. Unfortunately, there is no experimental data published for hamster Pgp to compare with the Hill number obtained by simulation. For reference, $IC_{SS}^{ATP}$ for the closely-related mouse Pgp was reported to be $18 \mu M$, with $n = 1.7$ [32]. Since Eqs. 16 and 17 describe with more accuracy the turnover rate and trapped fraction, they should be used to set the value of $K_{d}^{V_i}$, rather than Eqs. 1 and 2, as was done in the previous section.

![Figure 8. Steady-state simulation of the PE Alternating Cycle.](image)

(A) ATPase activity. Semi-log plot of ATP turnover rate (symbols) from the evaluation of $v_{SS,k_{C}}$ with $C_{SS} = \langle [ATP] \rangle$, 0, 0. The line is the best fit to a hyperbolic equation. (B) Inhibition by ADP. Double-reciprocal plots for ATP turnover rate from the evaluation of $v_{SS,k_{C}}$ with $C_{SS} = \langle [ATP] \rangle$, 0, 0) for $[ADP] = 0$ (red), 250 $\mu M$ (green), 500 $\mu M$ (yellow) and 1000 $\mu M$ (blue), with ATP concentration up to 100 $\mu M$. Inset: Double-reciprocal plots with ATP concentrations ranging upwards from 100 $\mu M$. Values of $k_i$ are given in Tables 2 and 3.

### Table 3

| Species | Reaction | Rate Constant |
|---------|----------|---------------|
| $P$ | $k_{p}$ | $k_{p}$ |
| $E_{ATP}$ | $k_{s}$ | $k_{s}$ |

![Figure 9. ATP dependence of several variables according to the PE Alternating Cycle.](image)

Semi-log plots of the steady-state ATP dependence of the normalized concentrations of (i) one-nucleotide species (red): $[E_{ATP}] + [F_{ATP}]$ with $C_{SS}([ATP],0,0,0)$ (ii) two-nucleotide species (brown): $[E_{ATP}] + [F_{ATP}]$ with $C_{SS}([ATP],0,0,0)$ (iii) bare enzyme (green): $[P]$ with $C_{SS}([ATP],0,0,0)$ and the relative hydrolytic activity, by evaluating $v_{SS,k_{C}}$ for (iv) ADP inhibition (pink): $C_{SS}([ATP],1000,0)/C_{SS}([ATP],0,0,0)$ (v) $P_i$ inhibition (yellow): $C_{SS}([ATP],0,200,0)/C_{SS}([ATP],0,0,0)$ and the normalized trapped fraction, by evaluating $T_{SS,k_{C}}$ for (vi) trapped species (blue): $C_{SS}([ATP],0,0,0)/C_{SS}([ATP],0,0,0)$ (vii) $P_i$ protection of $V_i$-trapping (black): $C_{SS}([ATP],0,0,0)/C_{SS}([ATP],1000,0,0)$ Concentration values for $C_{SS}$ are given in $\mu M$ except for $P_i$, which are in mM. Values of $k_i$ are given in Tables 2 and 3.

$[P_i] = 0.5 \mu M$. 

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adaptation of the basic alternating cycle proposed by Senior et al. [25] (grey cycle and trapping reaction with $V_i$, (ii) the priming reaction with ATP (blue reactions), and (iii) the priming reaction with ADP and a pathway for the release of ATP from the two-nucleotide trapped species (red reactions), by an independent pathway different from the catalytic reactions. The model for the Extended Alternating (Catalytic) Cycle was simulated only by numerical methods, using the rate constants in Tables 2, 3 and 4.

Figure 11A presents the time-course of the concentration of total trapped species during exposure to $V_i$ with ATP or ADP. Here, there is a noticeable difference in the rate of accumulation of both ATP and ADP trapping, Vi and ATP, by the pathway $E_{ATP}$ and ADP, trapped species (red reactions), by an independent pathway different from the catalytic reactions. The model for the Extended Alternating (Catalytic) Cycle was simulated only by numerical methods, using the rate constants in Tables 2, 3 and 4.

**Figure 11A** presents the time-course of the concentration of total trapped species during exposure to $V_i$ with ATP or ADP. Here, there is a noticeable difference in the rate of accumulation of both ATP and ADP trapping, Vi and ATP, by the pathway $E_{ATP}$ and ADP, trapped species (red reactions), by an independent pathway different from the catalytic reactions. The model for the Extended Alternating (Catalytic) Cycle was simulated only by numerical methods, using the rate constants in Tables 2, 3 and 4.

In addition, it was interesting to investigate the effect of an additional pulse of ATP during the recovery phase. According to the model, in the absence of $V_i$ the main trapped species is depleted by two possible routes: $E_{ADP} \xrightarrow{k_{a1}ATP} E_{ATP}$ (and the F-form equivalent). This low rate constant for ATP association, $K_{Vi}$, agrees with the high $K_{ATP}$ for the given $k_{a1}$, in turn constrained as mentioned above. All this assumes that binding of ATP is the rate-limiting step in the forward recovery pathway, $E_{ATP} \xrightarrow{k_{a1}ATP} E_{ATP}$, which is in concordance with the relatively high setting of $k_{\sim 5}$, constrained by the observed fast trapping and a pM value for $K_{a1}$, since $k_{\sim 5} = k_{5}k_{V}^{F}$. 

**Discussion**

Understanding the catalytic cycle of Pgp is essential to elucidate its transport mechanism. In spite of the efforts of several research groups over many years in providing good quality experimental data, no detailed kinetic analysis has yet been carried out. Consequently, some puzzling features of the system still remain unexplained, including: cooperativity of ATP hydrolysis at low ATP concentrations; mixed inhibition of ATPase activity by P; the steep concentration dependence observed for $V_i$ trapping with ADP/ATP; the kinetics of $V_i$ release from the trapped species; the kinetics of $V_i$ trapping with ADP; the relative $IC_{50}$ values for $V_i$ trapping using ATP/ADP; protection from ATP-trapping by P, and the detection of one-nucleotide trapped species. In this work, we present a quantitative evaluation of the currently accepted models for ATP hydrolysis and $V_i$ trapping, and assess their ability to explain the accumulated biochemical data. Using analytical and numerical methods, we evaluated the steady-state and the temporal behavior of the two main observable variables, the rate of ATP hydrolysis and the concentration of trapped enzyme. Thus, the basic reaction scheme for hydrolysis proposed by Urbatsch et al. [23], and its implementation in the Alternating Catalytic Cycle [25], were tested for their ability to reproduce the kinetic behavior of these variables.

The success and applicability of this mode of analysis depends critically on the set of kinetic parameters (rate constants) employed. Since such kinetic data does not currently exist, we established a coherent collection of rate constants that simultaneously matched both steady-state and temporal courses of all phenomenological and known thermodynamic properties describing catalysis and $V_i$ trapping. This self-consistent set of
parameters was obtained using the reciprocal constraints that impose: (i) the parameters that describe ATPase activity, i.e. \( k_{cat}, K_m \) and Hill number \( n \); (ii) reference values of \( K_d \) for nucleotides and Pi; (iii) the kinetics and phenomenological \( K/K_{IC_{50}} \) of products (ADP and P) and inhibitors (Vi) for hydrolysis and/or trapping; and (iv) the temporal course of Vi trapping and post-trapping recovery of ATPase activity (which is invaluable). It should be noted that some of these parameters are species-dependent. For example, \( \tau_{obs} \) for trapping with Vi using ADP for mouse Pgp (ABCB1b/Mdr3) is an order of magnitude slower than that for hamster Pgp [32]. In this regard, Table 1 compiles most of the parameters and observables reported for hamster Pgp (ABCB1a/Mdr1).

### The Steady-State Properties of the Elemental Cycle

As shown in Results, the output of this model is in agreement with the basic properties exhibited by an isolated half-cycle of ATP hydrolysis with respect to ATP dependence and competition by ADP. Our set of rate constants reported: (i) a high Michaelis constant \( (K_m \approx 600 \text{nM}) \) which, in combination with the relatively slow catalytic rate \( (k_{cat} \approx 10^{-5} \text{s}^{-1}) \), results in a low effective bimolecular rate constant \( k_{cat}/K_m = 1.6 \times 10^4 \text{M}^{-1} \text{s}^{-1} \); (ii) inhibition of ATPase activity by ADP at sub-mM levels \( (K_{ADP} \approx 500 \text{µM}) \); (iii) inhibition of ATPase activity by Pi at high mM levels \( (K_{Pi} \approx 200 \text{mM}) \); (iv) inhibition of ATPase activity by Vi at µM levels \( (K_{Vi} \approx 3 \text{µM}) \); (v) nucleotide dependence of trapping at µM levels. All of these values are the same order of magnitude as those reported in the literature for verapamil-activated Pgp (Table 1).

However, this model could not account for either the mixed-type inhibition exhibited by Pi, or for the observed ATP dependence of its protective effect on Vi trapping [14,23]. Analysis of the steady-state expression in this model (Eq. 1) revealed that \( K_{Vm}^{app} \) and \( k_{cat}^{app} \) can be described compactly according to

\[
K_{Vm}^{app} = \frac{[ADP]_t f(P_i)_t + K_m}{g(P_i)_t} \quad \text{when } [V_i] = 0 \quad (23)
\]

\[
k_{cat}^{app} = \frac{k_{cat}}{g(P_i)_t} \quad \text{when } [V_i] = 0 \quad (24)
\]

where \( f \) and \( g \) are functions of \([P_i]\) and the vector \( \mathbf{k} \). Thus, in the absence of ADP, the ratio between both parameters at any \( P_i \) concentration would be constant. However, in the presence of ADP in the reaction medium, the numerator of Eq. 23 is not reduced to \( K_m \), so the slope of the double-reciprocal plot is dependent on inhibitor concentration, a characteristic of mixed-type inhibition, as reported by Urbatsch et al. [23]. However, the explanation for the inhibition they observed is highly unlikely to be ADP accumulation following hydrolysis, since Pgp has a low catalytic rate, and the ATP concentration was kept constant during the experiment by a regenerating system.

Analysis of trapping with ATP/ADP uncovered another discrepancy between the output of the modeled Elemental Cycle and experimental evidence. According to Eqs. 11 and 12, at saturating Vi concentration the IC\(_{50}\) values of both nucleotides are defined by

\[
IC_{50}^{ATP} = \frac{K_{Vm}}{1 + \frac{[V_i]}{K_{Vi}}}
\]

\[
IC_{50}^{ADP} = \frac{K_{dADP}}{1 + \frac{[P_i]}{K_{Pi}}}
\]

Considering that (i) the numerators follow the relationship \( K_{Vm} > K_{dADP} \) and (ii) \( K_{Vi} \) is always > \( K_{Pi} \), since \( K_{Pi} = \alpha \beta K_{Vi} \) (Eq. 4d) and \( \alpha \beta = 1 + \frac{k_{4}}{k_{3}} + \frac{k_{4}}{k_{6}} > 1 \) (Eq. 5) for any value of the rate constants, the model cannot reproduce the experimental observation that \( IC_{50}^{ADP} > IC_{50}^{ATP} \) for any Vi concentration. To match the reported data \( K_{dADP} \) would need to be \( \geq 3K_m \). Additionally, the steeper concentration dependence reported experimentally [23] obviously reflects the binding of two nucleotides in the full catalytic.
cycle, and is in contrast with the Hill number of 1 obtained from the Elemental Cycle.

The relationship between \( P_i \) and \( V_i \) also revealed an additional element that makes the Elemental Cycle unsatisfactory. By simultaneously setting primary properties, such as \( K_i \) and \( K_{ji} \) from ATP hydrolysis and \( IC_{50} \) for trapping with both ATP and ADP, for a given set of other fundamental properties (especially \( K_m \) and \( K_{ADP} \)), it was impossible to mimic the reported relationship between these two oxoanions. The \( K_i \) values for trapping with ADP and ATP reported by the simulation were half of the values obtained experimentally. These values could not be matched without changing the other reported properties, that is by (i) increasing the competitive capacity of \( P_i \) (decreasing \( K_i \)); this change increases the \( P_i \) dependence of ATPase activity (i.e. by decreasing \( K_{ji} \) for activity), or (ii) decreasing the competitive capacity of \( V_i \) (increasing \( K_{ji} \)); this change affects the \( IC_{ATP} \) and \( IC_{ADP} \) for trapping.

The Temporal Behavior of the Elemental Cycle

Several considerations indicate that the observed slow kinetics of ADP trapping cannot be used to estimate the rate of ADP binding, as suggested by Urbatsch et al. [23], since this would yield \( k_4 \approx 1.2 \times 10^{-3} \text{M}^{-1} \text{s}^{-1} \). Such a low value for \( k_4 \), for the given \( K_{ATP} \) \( = 500 \text{ M} \), would make ADP dissociation the rate-limiting step for ATP hydrolysis, even if \( K_{ADP} \), is as high as 1.5 M. In this regard, decreasing \( k_4 \) below 0.04 s \(^{-1} \) (keeping the other rate constant) has a profound effect on the catalytic cycle, decreasing the turnover rate and \( K_m \) to unacceptable values. There is now ample consensus that catalysis is rate-limited in a concerted way, that is to say, there is no particular limiting step [18,35]. This can be rationalized if \( k_4 \) is quite similar to \( k_2 \), as long as the Pi dissociation rate is large (\( k_{-3} \gg 1 \text{ s}^{-1} \)), a requirement that is fulfilled due to the low affinity of \( P_i \) for EADP (and FADP). Thus, the steady-state turnover rate would be limited only for the steady-state \([E_{ATP}] \) and \([F_{ATP}] \), which are in turn dependent on \([ATP] \).

The Temporal Behavior of the Alternating Cycle

In the case of ADP binding, it is not possible to incorporate additional unimolecular steps into the Alternating Cycle (as previously suggested [23]) without either affecting the overall \( K_{ADP} \) while preserving the effective forward rate, or affecting the overall forward rate while preserving the overall \( K_{ADP} \). Nevertheless, Urbatsch et al. [32] considered fast binding of ADP followed by slow isomerisation but, again, inside the normal ATPase pathway. Our proposal on this issue, incorporated in the Extended Alternating Cycle, came from considering an alternative pathway for ADP binding (see the red reactions in Figure 2) outside the regular hydrolysis pathway. Thus, for \( V_i \), trapping, by either the fast pathway using ATP or the slower pathway using ADP, the final intermediates are the same, \( E_{ATP}V_i \) and \( F_{ATP}V_i \). This is the case since for the ATP pathway, the equilibrium \( E_{ATP}V_i \rightleftharpoons E_{ATP}V_i \) (and the F-form equivalent) is almost completely shifted toward the left (i.e. \( k_{4a}[ATP]/k_{1a} << 1 \)). Moreover, when the pulse of \( V_i \) and ATP is off (i.e. when ligand is removed), a rapid transition takes place toward the one-nucleotide trapped species (with \( k_{-1a} = 1 \text{ s}^{-1} \)). Thus, \( E_{ATP}V_i \) and \( F_{ATP}V_i \) would be the trapped species present in the gel filtration column eluate, as observed experimentally [23].

Both one- and two-nucleotide trapped species have been captured for hamster Pgp, depending on the nucleotide analog and inhibitor employed. In the presence of fluoroaluminate (AlF \(_4\)), Sankaran et al. [36] identified two nucleotides as trapped/bound [ADP/ATP or 8-azido-ADP/8-azido-ATP] when Pgp was incubated with ATP or 8-azido-ATP. In contrast, only ADP/8-azido-ADP was trapped in the presence of V, Beryllium fluoride (BeF \(_2\)) behaves similarly to V, in combination with nucleotides/8-azido-nucleotides [37]. Thus, the geometry of the transition state, dictated by the divalent cation, the inhibitor and the nucleotide analog used, determines the properties of the NBDs and the interaction between them, (i.e. \( K_{ADP} \)).

The inclusion of an independent pathway for ADP binding thus offers important advantages in explaining the cycle of catalysis and trapping. However, a complete reaction pathway should, in principle, consider sequential binding of two ADP molecules, as in \( P \rightleftharpoons E_{ADP} \rightleftharpoons E_{ADP} \) (and the F-form equivalent), in the same way that the PE Alternating Cycle proposes binding of two ATP molecules. Indeed, Pgp can bind two ADP (one in each NBD) in the absence of ATP. Qu et al. [38] reported the binding of two TNP-ADP molecules to Pgp by fluorescence titration, and Tombline et al. [34] found a Hill number of 1.7 for ADP binding to Pgp catalytic mutants. In addition, the ADP dependence of \( V_i \) trapping displayed cooperativity [23]. However, the species \( E_{ADP} \) and \( F_{ADP} \) can only be formed by incubation of Pgp with ADP alone, and thus they will not exist during the physiological catalytic cycle. Thus, the existence of distinct trapped species depending on the nucleotide used might account for the differential sensitivity to collisional quenching observed for Pgp trapped with ATP compared to ADP [39].

In our simulation, the unusually small values assigned to the rate constants for the trapping pathways [(i.e. \( k_{5a} \) and \( k_{5b} \) Table 4) should be noted: association rate constants for ligand-enzyme interactions are normally in the range \( 10^{-3} - 10^{-5} \text{M}^{-1} \text{s}^{-1} \). However, these values were set in order to reproduce, within the minimal reaction scheme, the kinetic behavior exhibited during trapping and release experiments. For example, consider \( V_i \) release in the presence of ATP by the path \( E_{ATP}V_i \rightleftharpoons E_{ATP}V_i \rightarrow E_{ATP}V_i \); the outcome is that the ATP dissociation constant was effectively set to a high value, \( K_{ATP} \approx 300 \text{M} \). The setting of \( k_{5b} \) to a low value (the rate-limiting step) was due to the setting of \( k_{5a} \), to a high value, which was in turn based on kinetic analysis of the Elemental Cycle. As mentioned above, it is feasible to include additional steps in \( V_i \) release, \( E_{ATP}V_i \rightarrow E_{ATP}V_i \rightarrow E_{ATP}V_i \), to allow assigning more reasonable values to these rate constants. The \( k_{5} \) step, which explains slow trapping by ADP, can also be split into several conformational steps. Even ADP association with the bare enzyme can be slow due to the absence of constraints imposed by \( k_{5a} \) in the regular catalytic pathway. In this regard, we found up to five transitions in TNP-ADP binding to Pgp under pseudo-first order conditions, with the observed time constants spanning 5 orders of magnitude, ranging from ms to tens of seconds [40].

The Concept of Alternating Catalysis

Alternating catalysis, which was originally proposed by Senior et al. [25], integrated two Elemental Cycles in tandem. It arises because of a mutual interaction between the two Pgp halves that allows only one NBD to be active for a particular protein conformation (i.e. NBD1 for E, NBD2 for F). Consequently, because binding of a second ATP to NBD2 is required to enable NBD1 to carry out hydrolysis (and vice versa), catalysis alternates between two Elemental Cycles. This characteristic is the crucial distinction between this mechanism and the Sequential Mechanism proposed.
by Sauna and Ambudkar [30], where alternation of the two
Elemental Cycles has its origin in the nature of the ATP binding step,
rather than the hydrolytic step. Thus, for the latter model, the
presence of ATP bound at a particular NBD is proposed to
prevent binding of a second ATP at the other NBD. Biochemical
and structural evidence supports the existence of a ternary Pgp
complex with two nucleotides bound; the currently accepted
model of catalysis is that each NBD carries out the catalytic cycle in turn,
enabled by the complementary NBD with ATP bound.

In the Alternating Cycle, during steady-state activity of the enzyme,
at least one molecule of ATP is always bound (see Figure 2, grey cycle); each ATP molecule to be hydrolysed must bind to a
previously formed Pgp:ATP complex. However, for a newly
synthesized Pgp molecule in the cell, or at the beginning of an in
vitro ATPase assay, the protein does not have any bound
nucleotide. Thus, the priming reaction \( P \xleftrightarrow{ATP} E^{ATP} \) (and its
equivalent for the F-form) must necessarily occur. This step has
possibly been ignored in the past because it is “obvious”, but it is
necessary to include it explicitly to provide a pathway for the
protein to enter the catalytic cycle. As discussed below, this
additional binding reaction generates changes in the ATP
dependence of any measured variable, and suggests some new
concepts about the catalytic mechanism. The simple Elemental Cycle
simulation obviously cannot report interaction in the nucleotide
dependence of any variable for the intact Pgp, since only one
nucleotide is involved in the cycle. However, for the Alternating Cycle, the observation of \( n\geq1 \) for in vitro trapping with ATP arises
because of nucleotide priming reactions (in the case of in vitro
trapping with ADP, the simulation still reported \( n=1 \), since only
one ADP binding event was considered in this case). When simulating the PE Alternating Cycle, the value of the Hill number
obtained for trapping is dependent on the ratio between the two
ATP affinities and the type of coupling between the NBDs. Thus,
for sequential binding of two ATP molecules, the Hill number
ranges from: (i) \( n=2 \), when the catalytic sites present no binding
interaction \( K_{dATP} = K_{dATP}^{\text{PE}} \) but show interdependence at the
hydrolysis step (alternating catalysis, mutual exclusion of hydrolytic activity); (ii) \( 1<n<2 \), for a negative binding interaction
\( K_{dATP}^{\text{PE}} > K_{dATP} \) with again, inter-dependence of hydrolysis (e.g.
alternating catalysis); and (iii) \( n=1 \), for mutual exclusion in the
binding \( K_{dATP} = \infty \) i.e. after binding of the first ATP, binding of a
second ATP cannot occur) and independent hydrolysis; which is
the case for either uncoupled/isolated half-molecules (the Elemental Cycle) or the Sequential Mechanism (Elemental Cycles in tandem). For
Pgp undergoing a complete catalytic cycle at both NBDs, as
already discussed, option (iii) is discarded. However, due to the
absence of any quantitative reports of the value of \( n \) for wild-type
hamster Pgp, it is not possible to rule out either of the first two
possibilities based on trapping experiments. However, several
pieces of evidence point towards the second option (a negative
binding interaction):

(i) The Sequential Mechanism [30] proposed allosteric control of
the ATP binding affinities of the two NBDs. In this model, the
alternating feature of the hydrolysis arises from the impossibility of a two-nucleotide species due to
ramific reduction in the binding affinity for a second nucleotide
when one is already bound. Evidence was presented that
correlated decreased affinity for drug with decreased affinity
for nucleotide, thus, accounting for the release of both at the
end of the catalytic cycle. Viewing this proposal using our
model, the species \( E^{ATP} \) must have low ADP affinity in the
empty NBD (i.e. NBD2) to account for release of ADP from

(ii) The observed Michaelis-Menten (\( n=1 \)) behavior of the ATP
dependence of hydrolysis requires either complete indepen-
deance \( K_{dATP} = \infty \) no binding of a second ATP) or a higher
priming reaction affinity \( K_{dATP}^{\text{PE}} < < K_{dATP} \). Although high
affinity binding of ATP has not been reported, this is not
conclusive, since the various reports are imprecise or incomplete. Plots of the nucleotide dependence of ATP
hydrolysis by Pgp have often started from a relatively high
nucleotide concentration (e.g. 50 \( \mu \)M), thus missing details
of the low concentration part of the curve. It should be
noted that the inclusion of a high affinity priming reaction
generates curves for ATP dependence that deviate only very
slightly from the single-binding model, so that it would only
be perceptible in either log or log-log plots. In addition,
the low concentration part of the curve could only be taken into
account using a weighted fitting to a Hill model; a non-
weighted simple Michaelis-Menten fitting would miss the
high affinity component.

(ii) An interesting report by Buxbaum [33], which measured
hydrolysis of ATP in the \( \mu \)M range, reported significant
deviation from hyperbolic behavior. Upward curvature in the
log-log plot was observed at low ATP concentrations,
with a breakpoint at ~10 \( \mu \)M, which can only be explained
by interaction between the NBDs during catalysis. In
addition, the author reported that activation of ATP
hydrolysis by verapamil occurred only at high ATP
concentration, which might be reconciled with our model
by adding a priming cycle for ATP hydrolysis (i.e. hydrolysis
of the one-nucleotide species) uncoupled from drug transport.

The essential steps in the alternating mechanism proposed by
Urbatsch et al. [32] are depicted in the cartoon in Figure 12A.
The ATP binding reaction is conceived as a random process,
producing the two-nucleotide intermediate (C) without any
distinction in their binding affinities. Subsequently, this interme-
diate chooses a pathway toward either D0 or Dc, depending on
which NBD last hydrolyzed ATP. This model requires the
intermediate C to have some type of “memory”, i.e. C must
possess some intrinsic difference based on the last hydrolytic event,
for example, a slight difference in the forward rate (C\( \rightarrow \)D)
between NBD1 (N-end) and NBD2 (C-end). However, by
definition, C must be identical regardless of the branch used for
the priming binding step, so that the next step would have to be
randomly selected. This places Senior’s Alternating Mechanism in an
awkward position: in the forward step from C, there is no
guarantee of alternation of the two half-cycles.

In contrast, our proposal for the Alternating Cycle (Figure 12B)
considers sequential ATP binding with decreased affinity for the
second nucleotide, to produce distinct two-nucleotide intermedi-
ates, \( C_N \) and \( C_C \). In this model, alternation is guaranteed since
there is no common intermediate; there is no need to propose
the existence of memory for any species. The model in Figure 12B
is equivalent to that shown in Figure 2, where one branch (blue)
corresponds to the E-form of Pgp, and the other (red) to the
F-form, and the intermediate A corresponds to the P-form. Thus, the
release of ADP and the transition between kinetics forms in Figure 2 (E ↔ F), are represented by the transitions Fₚ ↔ Bᵥ and Fᵥ ↔ B₀ in Figure 12B.

In summary, in our implementation of the Alternating Cycle in Figure 12B, the needed asymmetry for the alternation of the two paths is structural in origin (it is contained within the overall cycle), and arises from the reciprocal negative allosteric interaction between the NBDs. On the other hand, Senior’s Alternating Cycle shown in Figure 12A is functional in origin (it is facilitated by the functioning of the cycle), since it depends on the “memory” of a particular intermediate for the previous hydrolytic event. This feature ultimately arises because the model does not consider the priming reactions, and considers only the cycling part of the scheme.

The Occluded State

The concept of occlusion proposed by Tombline and Senior [41] can be easily supported in our current model, as depicted in Figure 12B by the transitions C ↔ D. For this, the conformational transition between the non-occluded (C) and occluded (D) two-nucleotide species would be represented by $E_{ATP} \xrightarrow{k_i \cdot ATP} E_{ATP}$ in the kinetic schemes, where $E$ denotes the non-occluded state and $\bar{E}$ the occluded state, with equilibrium constant $K_i$. This transition is not a binding event, since there is no direct exchange (association or dissociation) of ATP, so that the apparent ATP affinity of the occluded species ($K_{i\cdot ATP}$) would, in fact, be the overall ATP dissociation constant for the second nucleotide, as represented by the serial equilibria, $E_{ATP} \xrightarrow{k_i \cdot ATP} E_{ATP} \xrightarrow{k_k \cdot ATP} E_{ATP}$, with $K_{i\cdot ATP} = K_{k\cdot ATP} (1 + K_i)^{-1}$. Thus, as occlusion progresses in the forward direction ($K_i > 1$), the apparent ATP binding affinity is significantly increased relative to the true “microscopic” binding affinity ($K_{i\cdot ATP} < K_{k\cdot ATP}$). However, this additional transitional step is not necessary to account for the experimental data reported with Pgp mutants and ATP analogs, as explained below.

According to our interpretation, the work of Tombline et al. with Pgp mutants [34] might correspond to a pseudo-equilibrium binding titration of the bare enzyme, due to impairment in the hydrolytic rate constant, which reduced $k_3$ by a factor of 1000. Figure S2A matches the steady-state distribution at various ATP concentrations of the intermediates $E_{ATP}$ and $F_{ATP}$, which closely matches the equilibrium $E_{ATP} \xrightarrow{k_i \cdot ATP} E_{ATP} \xrightarrow{k_k \cdot ATP} E_{ATP}$ (and the F-form equivalent). By decreasing both rate constants of the priming reaction ($k_0$ and $k_{-0}$, keeping $K_{i\cdot ATP}$ constant) the experimental data of Tombline et al. [34] could be simulated. After removal of free ligands, the reactions that describe the system, $P \xrightarrow{k_{-0}} E_{ATP} \xrightarrow{k_i \cdot ATP} F_{ATP} \xrightarrow{k_k \cdot ATP} E_{ATP}$ (and the F-form equivalent) predict occlusion of the nucleotide (equivalent to trapping without V₁). This arises mainly from formation of the species $E_{ATP}$ (and $F_{ATP}$) due to slower conversion of $E_{ATP}$, and also increased formation by dissociation of two-nucleotide species $E_{ATP}$ (and the F-form equivalent), which built up to a higher steady-state concentration because of greatly reduced hydrolysis. We decreased $k_0$ and $k_{-0}$ by 1000-fold for the Pgp mutants and assumed that after passage through a gel filtration column (~30 s) almost all of the two-nucleotide species become one-nucleotide species (since $k_{-1} = 1000 \cdot k_{-0} \approx 20000$).

Figure S2B shows the fraction of Pgp with retained nucleotide (i.e. occluded species) at various ATP concentrations, and reports an overall affinity for ATP ($K_{i\cdot ATP}$) quite close to $K_{d\cdot ATP}$, in the uM range. In addition, the variable effect of several drugs on the steady-state stoichiometry of occlusion at a fixed nucleotide concentration [27] might be accounted for by a differential effect on $K_{d\cdot ATP}$ (see Figure S3).

We recently reported that the binding to Pgp of the poorly-hydrolysable analog ATPS exhibits a biphasic isotherm, with $K_{i\cdot ATPS} = 6 \mu M$ and $K_{d\cdot ATPS} = 740 \mu M$ [29], with the highest affinity binding component assumed to correspond to the occluded state. However, our interpretation based on the current model is that $K_{i\cdot ATPS}$ may correspond to the affinity of the bare enzyme ($K_{d\cdot ATP}$, see Figure S3). This would account for the $K_{i\cdot ATPS}$ of 6 uM observed for the inhibition of the ATP hydrolysis by ATPS [29], corresponding to competition with ATP for the high affinity site ($K_{d\cdot ATP}$) of bare Pgp.

In consequence, our model is compatible with the proposal of occlusion; but differs from it conceptually in the following way. The occluded state ($E_{i\cdot ATP}$) identified experimentally has a tightly bound ATP (uM affinity) committed to hydrolysis, while a second molecule is bound to the complementary NBD. In our interpretation, this intermediate ($D_{NBD/C}$ in Figure 12A) corresponds to the species $E_{i\cdot ATP}$ and $F_{i\cdot ATP}$ in Figure 8; it has one NBD with high affinity (e.g. NBD1 and NBD2 for the E and F isoforms, respectively), and is represented by intermediates $C_{NBD}$ in Figure 12B. That is to say, in our model it is not necessary to include a conformational transition to the occluded state, since the high affinity site exhibited by this state actually corresponds to the site that bound the first nucleotide molecule to the bare enzyme. Consequently, occlusion would not necessarily reflect an increase in affinity of the NBD with ATP already bound, following binding of a second ATP in the complementary NBD. Rather, it might correspond to the conformational change that enables the high affinity NBD to hydrolyze the committed nucleotide, thus preparing the enzyme for the hydrolytic step. This could occur concurrently or after the binding of a second ATP, represented in Figure 12B as the transition $C_{NBD} \rightarrow D_{NBD/C}$. The occluded state is easily incorporated into the kinetic scheme in Figure 2 as the transitions $E_{i\cdot ATP} \xrightarrow{k_i \cdot ATP} F_{i\cdot ATP} \xrightarrow{k_k \cdot ATP} E_{i\cdot ATP}$, however, as indicated previously, from a kinetic point of view it is not necessary to include this feature in our model.

Conclusions

The detailed analysis provided in this work underscores the fact that the mechanism underlying the kinetics of Pgp-mediated ATP hydrolysis must be much more complex than that proposed in previous models. Our goal was to incorporate the wealth of experimental data accumulated for hamster Pgp into a consistent kinetic simulation of the catalytic cycle. Implementation of the Elemental Cycle in the Alternating Mechanism (as originally proposed by Senior’s group [25]) adequately explains (i) the time-domain and steady-state experimental data for ATP hydrolysis with respect to ATP, ADP and V₁ concentrations; (ii) the steady-state experimental data for ATP/ADP dependence of V₁ trapping; and (iii) the kinetics of V₁ trapping with ATP. However, it fails to satisfactorily explain (a) the effect of P on ATPase activity; (b) the relationship between $IC_{50}$ for ATP/ADP on V₁-trapping; (c) cooperativity of ATP hydrolysis at low ATP concentrations; (d) the observed protective effect of P on V₁-trapping with respect to the $IC_{50}$ for ATP/ADP; (e) the steep concentration dependence observed for V₁ trapping with ADP/ATP; (f) the kinetics observed for V₁,
trapping with ADP; (g) the kinetics observed for Vi release from the trapped species; and (h) detection of species with only one trapped nucleotide. Development of the Extended Alternating Cycle allowed us to include additional kinetic steps to account for most of the deficiencies (c)-(h) of the original model (however, observations (a) and (b) still remain unexplained). Figure 9 summarizes the ATP dependence of several biochemical variables in the PE Alternating Cycle of Pgp, according to the parameters given in Tables 2 and 3. This proposed model introduces both priming and trapping reactions into the kinetic scheme, and is able to account for the observed high affinity of Pgp for ATP without any reference to the occluded state, thus avoiding assigning special properties to any intermediate in the cycle. A new interpretation of the occlusion phenomenon also emerges from the model. Future work will be needed to model a comprehensive reaction scheme to explain the complete data-set of biochemical observations.

Supporting Information

Figure S1 Inhibitory effect of ADP on Pgp ATPase activity for the Elemental Cycle. (A) 3D plot from the evaluation of $V_{SS,kC}$ with $C_{SS} = \langle [ATP],[ADP],0,0 \rangle$. (B) Double-reciprocal plot from the evaluation $V_{SS,kC}$ with $C_{SS} = \langle [ATP],[ADP],0,0 \rangle$ for $[ADP] = 0$ (red), 250 (green), 500 (yellow) and 1000 μM (blue), with ATP concentrations ranging upwards from 10 μM. Values of $k$ are given in Table 2. (TIF)

Figure S2 ATP dependence of the concentration of several intermediates in the PE Alternating Cycle for catalytic mutants of Pgp. Based on Figure 2 and the values of $k$ given in Tables 2 and 3, but substituting the following values: $k_0 = 0.01 \mu M^{-1}s^{-1}$, $k_{--} = 0.05 s^{-1}$ and $k_2 = 0.02 s^{-1}$ (a 1000-fold impairment in the original rate constants). (A) Concentration of intermediates: $[P]$ (blue), $[E_{ATP}^{[TP]}] + [F_{ATP}^{[TP]}]$ (red), and $[E_{ATP}^{[TP]}] + [F_{ATP}^{[TP]}]$ (green); (B) Fraction of Pgp with retained nucleotide, according to the function $R_{SS,kC} = ([E_{ATP}^{[TP]}] + [F_{ATP}^{[TP]}] + [F_{ATP}^{[TP]}])/[P]$, with $C_{SS} = \langle [ATP],0,0,0 \rangle$. The synthetic data from the model (blue symbols) were fitted to a Hill equation (red line), yielding $K_v = 5.1 \mu M$ and $n = 1.01$. (TIF)

Figure S3 Effect of altering the affinity of the priming reaction on retention of nucleotides for catalytic mutants of Pgp. $K_v^{TP}$ was altered by changing $k_{--}$, while imposing a 1000-fold impairment in the original rate constants ($k_0 = 0.01 \mu M^{-1}s^{-1}$ and $k_2 = 0.02 s^{-1}$). The fraction of intermediates with retained

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**Figure 9.** Summarizes the ATP dependence of several biochemical variables in the PE Alternating Cycle of Pgp, according to the parameters given in Tables 2 and 3. This proposed model introduces both priming and trapping reactions into the kinetic scheme, and is able to account for the observed high affinity of Pgp for ATP without any reference to the occluded state, thus avoiding assigning special properties to any intermediate in the cycle. A new interpretation of the occlusion phenomenon also emerges from the model. Future work will be needed to model a comprehensive reaction scheme to explain the complete data-set of biochemical observations.

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nucleotide was evaluated by $R_{SS|kC}$ (as defined in Figure S2) with $C_{SS} = \langle [ATP]_0, 0, 0, 0 \rangle$, relative to the retained fraction for the original $K_{ATP}^{TOT} = 5 \mu M$. Based on Figure 2 and the values of $k$ given in Tables 2 and 3.

(TIF)

**Figure S4** Simulation of the stoichiometry of trapped ATPyS based on the PE Alternating Cycle. ATP dependence of the stoichiometry of trapped nucleotide based on Figure 2, according to the function $Q_{SS} = \langle [ATP]_0, 0, 0, 0 \rangle + 2\langle [ATP]_0, 0, 0, 0 \rangle + 3\langle [ATP]_0, 0, 0, 0 \rangle |P|$, with $C_{SS} = \langle [ATP]_0, 0, 0, 0 \rangle$, for values of $k$ given in Tables 2 and 3, but considering $k_0 = 0.01 \mu M^{-1} s^{-1}$, $k_1 = 1 \times 10^{-4} \mu M^{-1} s^{-1}$ and $k_2 = 0.02 s^{-1}$ (a 1000-fold impairment in the original values). The synthetic data from the model (blue symbols) were fitted to a two-site binding model (red line), yielding $Q_{SS} = \frac{[ATP]_0}{5.02 + [ATP]_0} + \frac{[ATP]_0}{1199 + [ATP]_0}$ (TIF)

**Author Contributions**

Conceived and designed the experiments: MRL FJS. Performed the experiments: MRL. Analyzed the data: MRL FJS. Wrote the paper: MRL FJS.

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