Testing the Mechanism for the LSP Stability at the LHC

Pavel Fileviez Pérez, Sogee Spinner, and Maike K. Trenkel
Phenomenology Institute, Department of Physics, University of Wisconsin-Madison, WI 53706, USA
(Dated: January 15, 2013)

The lightest supersymmetric particle (LSP) is a natural candidate for the cold dark matter of the universe. In this letter we discuss how to test the mechanism responsible for the LSP stability at the LHC. We note that if $R$-parity is conserved, one should expect a Higgs boson which decays mainly into two right-handed neutrinos (a “leptonic” Higgs) or into two sfermions. The first case could exhibit spectacular lepton number violating signals with four secondary vertices due to the long-lived nature of right-handed neutrinos. These signals, together with the standard channels for the discovery of SUSY, could help to establish the underlying theory at the TeV scale.

**Introduction:** The Minimal Supersymmetric Standard Model (MSSM) is considered as one of the most appealing candidates for TeV scale physics since in this context one can protect the Higgs mass, there is a natural cold dark matter candidate of the universe if $R$-parity is conserved, it can accommodate electroweak baryogenesis, and one can achieve the unification of gauge couplings at the high-scale. For a review of Supersymmetry (SUSY) see Ref. [1].

The signatures of low-energy SUSY at the LHC depends on the conservation or violation of $R$-parity. This symmetry is defined as $R = (-1)^{2S + 3(B-L)}$, where $S$, $B$ and $L$ are the spin, baryon and lepton number, respectively. If $R$-parity is conserved the superpartners are produced in pairs and typical channels include multi jets, multi leptons and missing energy. The latter due to the LSP which might also be dark matter. When $R$-parity is broken single superpartner production is possible as well as observable lepton or baryon number violation at the LHC [2].

The origin of $R$-parity conservation or violation can be understood in TeV scale theories based on the $B-L$ gauge symmetry. It is well-known that if the Higgs breaking $U(1)_{B-L}$ has even $B-L$ charge, $R$-parity is conserved after symmetry breaking [3]. Testing this mechanism at the LHC requires an investigation of the properties of the $Z_{BL}$ neutral gauge boson, the right-handed neutrinos needed to define an anomaly free theory, and the new $B-L$ Higgses. This is the main goal of this work.

In this letter we study the properties of the Higgs sector of theories which explain the origin of $R$-parity conservation and find that there are two major types of models. In the first type the Higgses allowing for the stability of the LSP can decay mainly into two right-handed neutrinos (we call it the “leptonic” Higgs). We find that the $B-L$ Higgses could give rise to spectacular signals with four displaced vertices due to the long lifetime of right-handed neutrinos. See Fig. 1 for a naive representation of these signals. In the second type of model, the new Higgses can decay mainly into two sfermions where the final states depend on the SUSY spectrum. However, specific scenarios have peculiar signals with multi-leptons and multi-photons in the final states. Our results are relevant to understand the testability of the mechanism responsible for the LSP stability in low energy SUSY and together with the standard SUSY discovery channels, could help establish the underlying theory at the TeV scale.

**Theoretical Framework:** We begin by reviewing some details of the MSSM. As it is well-known, the superpotential is given by

$$W_{MSSM} = W_{RpC} + W_{RpV},$$

(1)

where $W_{RpC}$ is the $R$-parity conserving part,$\quad W_{RpC} = Y_u QH_u u^c + Y_d QH_d d^c + Y_e LH_d e^c + \mu H_u H_d,$

(2)

and

$$W_{RpV} = \epsilon LH_u + \lambda LLe^c + \lambda' QLd^c + \lambda'' u^c d^c,$$

(3)

contains the $R$-parity violating terms. The simplest way to imbide $R$-parity conservation into a gauge symmetry is through $B-L$ where the new gauge group is

$$SU(3)_C \otimes SU(2)_L \otimes U(1)_Y \otimes U(1)_{B-L}.$$  

Now the terms in $W_{RpV}$ are not allowed at the $B-L$ scale. Gauging $B-L$ requires the addition of three copies of right-handed neutrinos to satisfy anomaly cancellation, enhancing the superpotential to

$$W_{B-L} = W_{RpC} + Y_\nu LH_u \nu^c + W_{extra},$$

(4)

FIG. 1: Naive representation of the topology for the signals with secondary vertices and lepton number violation due to the existence of long lived right-handed Majorana neutrinos.
where the last term is dependent on the Higgs sector.

There are two simple Higgs sector that allow for $R$-parity conservation:

**Model I:** A pair of Higgses: $X, 	ilde{X} \sim (1, 1, 0, \pm 2)$ is added to the theory so that the extra term in the above superpotential becomes

$$W_{\text{extra}}^{(I)} = \mu_X X \tilde{X} + f \nu^C \nu^C X. \tag{5}$$

In this model $B - L$ is broken by the vevs of $X$ and $	ilde{X}$, and $R$-parity is an exact symmetry at the TeV scale. Due to the second term in the above equation, the neutrinos are Majorana fermions and the new physical Higgses, $X_1, X_2$ and $A_{BL}$, can decay at tree level into two right-handed neutrinos. These decays are the key to revealing the properties of the $B - L$ breaking Higgses, *i.e.* indicating if $R$-parity is really conserved at the TeV scale. In this case radiative symmetry breaking could explain the origin of symmetry breaking at the TeV scale [4].

**Model II:** $S, \tilde{S} \sim (1, 1, 0, \pm n_S)$ with even $n_S \neq 2$, are introduced and the extra term in the superpotential is

$$W_{\text{extra}}^{(II)} = \mu_S SS. \tag{6}$$

Here the neutrinos are Dirac fermions and the new physical Higgses, $S_1, S_2$ and $A_S$, do not couple to SM fields at tree level. These Higgses can decay at tree level into two fermions and give rise to peculiar signals in specific SUSY scenarios. It is important to mention that an odd $|n_S| \neq 1/2, 1$, will have higher-dimensional operators which will affect the stability of the LSP, although it may still live long enough to be a dark matter candidate.

**Symmetry Breaking:** In order to simplify the symmetry breaking discussion we introduce the generic fields, $\phi, \tilde{\phi} \sim (1, 1, 0, \pm n_\phi)$. Then, $\phi(\tilde{\phi})$ can be $X(\tilde{X})$ in Model I or $S(\tilde{S})$ in Model II. The relevant soft terms for our discussion are:

$$-\mathcal{L}_{\text{Soft}} \subset \left( a_L \bar{L}_i H \nu^C \right) \bar{B}^C B^C + \text{h.c.} + m_{BL}^2 |B^C|^2,$$

$$+ m_{B_L}^2 |\phi|^2 + m_{\tilde{B}_L}^2 |\tilde{\phi}|^2 + m_{\nu^C}^2 |\nu^C|^2, \tag{7}$$

where $B^C$ is the $B - L$ gaugino. Spontaneous $B - L$ breaking and $R$-parity conservation requires the vacuum expectation values (VEV) of $\phi$ and $\tilde{\phi}$ to be non-zero. Using $\langle \phi \rangle = v/\sqrt{2}$ and $\langle \tilde{\phi} \rangle = \bar{v}/\sqrt{2}$ for the VEVs, one finds

$$V = \frac{1}{2}|\mu_\phi|^2 (v^2 + \bar{v}^2) - b_\phi v \bar{v} + \frac{1}{2} m_\phi^2 v^2 + \frac{1}{2} m_{\tilde{\phi}}^2 \bar{v}^2$$

$$+ \frac{g_{BL}^2}{32} n_\phi^2 (v^2 - \bar{v}^2)^2. \tag{8}$$

Assuming that the potential is bounded from below we get:

$$2b_\phi < 2|\mu_\phi|^2 + m_\phi^2 + m_{\tilde{\phi}}^2, \tag{9}$$

while

$$b_\phi^2 > (|\mu_\phi|^2 + m_\phi^2) (|\mu_\phi|^2 + m_{\tilde{\phi}}^2), \tag{10}$$

is necessary for a nontrivial vacuum. Minimizing with respect to $v$ and $\bar{v}$ one gets

$$|\mu_\phi|^2 + m_\phi^2 - \frac{1}{2} m_{BL}^2 \cos 2\beta' - b_\phi \cot \beta' = 0, \tag{11}$$

$$|\mu_\phi|^2 + m_{\tilde{\phi}}^2 + \frac{1}{2} m_{BL}^2 \cos 2\beta' - b_\phi \tan \beta' = 0, \tag{12}$$

with $\tan \beta' = v/\bar{v}$ and $m_{BL}^2 = g_{BL}^2 n_\phi^2 (v^2 + \bar{v}^2)/4$. Notice that the minimization conditions are quite similar to the MSSM conditions.

**Higgs Sector:** The Higgs sector contains two extra CP-even neutral Higgs fields: $H_1$ and $H_2$, and one CP-odd Higgs, $A_\phi$, which this general notation will be replaced by the specific notation outlined in the model subsections. The eigenvalues in the CP-even neutral Higgs sector read as

$$m_{H_{1,2}}^2 = \frac{1}{2} \left( m_{A_\phi}^2 + m_{Z_{BL}}^2 \pm \sqrt{D} \right), \tag{13}$$

with

$$D = (m_{A_\phi}^2 - m_{Z_{BL}}^2)^2 + 4m_{Z_{BL}}^2 m_{A_\phi}^2 \sin^2(2\beta'), \tag{14}$$

and the mixing angle obeys the following relation:

$$\tan 2\alpha' = \frac{m_{A_\phi}^2 + m_{Z_{BL}}^2}{m_{A_\phi}^2 - m_{Z_{BL}}^2}. \tag{15}$$

Notice that in the limit, $m_{Z_{BL}}^2 \gg m_{A_\phi}^2$, one finds that

$$m_{H_1}^2 \sim m_{A_\phi}^2 \left( 1 - \sin^2(2\beta') \right), \tag{16}$$

$$m_{H_2}^2 \sim m_{Z_{BL}}^2 + m_{A_\phi}^2 \sin^2(2\beta'). \tag{17}$$

Then, assuming $g_{BL} \sim O(1)$ and the experimental limit, $m_{Z_{BL}}/g_{BL} > 3$ TeV [5], one expects two light Higgses, $H_1$ and $A_\phi$, and a heavy one, $H_2$, when $m_{A_\phi}$ is small: a technically natural limit as a massless pseudoscalar corresponds to an enhanced global symmetry of the Lagrangian.

**Production Mechanisms and Higgs Decays:** Testing these scenarios for $R$-parity conservation requires an understanding of how to produce the $B - L$ Higgses at the LHC and their decays. The following production mechanisms are possible: a) Single Production via Gluon fusion: $pp \to H_1$, b) Pair production: $pp \to Z_{BL} \to H_1 A_\phi$, c) Associated production: $pp \to Z_{BL} \to Z_{BL} H_1$ and d) $Z_{BL}$ boson fusion. The single production is quite model dependent while the associated production and the vector boson fusion are very small due to the experimental limits on the $Z_{BL}$ mass. Therefore, we focus mainly on the pair production, which also has the interesting property that while it is not a SUSY process, it is absent in minimal non-SUSY $B - L$ models. We postpone the study of the other production channels for a future publication [6].

The pair production cross section for Model I, $pp \to X_{1A_{BL}}$, versus the CP-odd scalar Higgs mass is shown in Fig. 2, using the MSTW2008 LO pdf at a central factorization scale $\mu = (m_{A_{BL}} + m_{X_1})/2$. Here, for illustration,
we show two different $Z_{BL}$ masses: 1 TeV (solid) and 2 TeV (dashed) (assuming $g_{BL}$ at its maximum allowed value in each case), and three different values for the Higgs mass, $m_{X_1} = 100$ GeV, 200 GeV and 400 GeV. This process also has a mild dependence on the SUSY spectrum through the $Z_{BL}$ width. All results are shown for center of mass energy of 14 TeV. Larger cross sections for larger values of $m_{X_1}$ (for $m_{X_1} + m_{ABL}$ below the $m_{Z_{BL}}$ threshold) correspond to larger value of $\tan \beta'$, a parameter that is uniquely determinable at each point on the curves. For details see [6]. This plot shows that when the pseudoscalar mass, $m_{ABL}$, is smaller than 500 GeV, the hadronic cross section can be above 1 fb for these input parameters and in the most optimistic region ($m_{X_1} < 200$ GeV and $m_{ABL} < 250$ GeV) can go as high as 100 fb indicating a large number of events. Cross sections for Model II do not simply scale as $n^2_3$ as it also effects the width of $Z_{BL}$, see [6].

With these values for the cross section we are now ready to study the possible decays in these models, focusing on tree-level two-body decays for $H_1$ and $A_\phi$ as the most accessible fields. In Model I the CP-even physical Higgs, $X_1$, can decay at tree level into two right-handed neutrinos, into two sfermions or into two $B-L$ neutralinos, while the CP-odd Higgs can decay into two right-handed neutrinos, two $B-L$ neutralinos, and $X_1$ and $Z_{BL}$. However, since the collider bounds on the $Z_{BL}$ mass are strong and we’re focusing on a light Higgs, the decays into two $Z_{BL}$s and sfermions are suppressed. Therefore, we are mainly interested in the decays into two right-handed neutrinos which would reveal the nature of the $B-L$ Higgses. Notice that in this case the right-handed neutrinos are Majorana fermions and their decays produce lepton number violating signals.

In Model II the physical Higgses, $S_1$, $S_2$ and $A_S$ do not have couplings to the fermions at tree level. Then, the CP-even Higgses can decay mainly into two sfermions or two $B-L$ neutralinos. The CP-odd Higgs can decay into $Z_{BL}^\pm$ and $S_1$ or two $B-L$ neutralinos. One possible interesting scenario corresponds to the case where $S_1$ can decay mainly into selectrons and $A_S$ through the three body decays, $A_S \rightarrow S_1(Z_{BL}) \rightarrow S_1e_j^+e_i^-$. The possible signals in this model depend of the particular SUSY spectrum. The simplest scenarios will be discussed in the next section.

Since in Model I the Higgses can decay mainly into two right-handed neutrinos, their properties are important when discussing signals at the LHC. The possible decays for $N$ are: $N \rightarrow W^\pm e^\mp, Z\nu, \nu h_i$, where $h_i$ are the MSSM Higgses. The partial width for these decays are proportional to the mixing between the light SM neutrinos and $N$. The relevant mixing matrix is given by

$$V_{LN} = V_{PMNS} m_1^{1/2} \Omega N^\dagger_1.$$  \hspace{1cm} (18)

Here $V_{PMNS}$ is the PMNS mixing matrix, $m = \text{diag}(m_{\nu_1}, m_{\nu_2}, m_{\nu_3})$ are the physical neutrino masses, and $\Omega$ is a complex orthogonal matrix, which conveniently parameterizes some of the unknown degrees of freedom of the neutrino sector. In Fig. 3 we show lines of constant decay length for the right-handed neutrinos in the right-handed neutrino mass spectrum for the left-handed neutrinos. Here we have used the central values for the atmospheric and solar mass squared difference, the tri-bimaximal ansatz and assumed $\Omega = 1$. As can be appreciated from Fig. 3, the right-handed neutrinos are long-lived in the full parameter space considered implying the existence of secondary vertices. For a detailed study of the right-handed decays see Ref. [7].
Signals at the LHC: In Model I we will focus on the light Higgs bosons scenario, with \( m_{X_1} > 2m_{N_1} \), which decay only into two right-handed neutrinos. This corresponds to the most optimistic case where one has lepton number violation through the right-handed neutrino decays. For single production of the \( B - L \) Higgs boson \( X_1 \), the following lepton number violating signals at the LHC are possible:

\[
pp \rightarrow X_1 \rightarrow N N \rightarrow e_i^± W^± e_j^± W^± \rightarrow e_i^± e_j^± 4j.
\]

Since the single production depends heavily on the SUSY spectrum we shift our focus to the pair production as the arena for testing the stability of the LSP. In this case one has

\[
pp \rightarrow Z_{BL}^* \rightarrow X_1 A_{BL} \rightarrow N N N N \rightarrow e_i^± e_j^± e_k^± e_l^± 8j,
\]

leading to four same-sign leptons and eight jets in the final state and allowing for observation of lepton number violation. These signals are even more spectacular once we consider the fact that the right-handed neutrinos are long-lived, which lead to four secondary vertices. The topology of these event are shown in Fig. 1.

We can perform a naive estimate to gain an appreciation for the number of events for this four same-sign leptons and 8 jets signal using a cross section of 100 fb and an integrated luminosity of 100 fb\(^{-1}\):

\[
N_{4e8j} \approx \sigma (pp \rightarrow X_1 A_{BL}) \times BR(X_1 \rightarrow N_1 N_1) \times BR(A_{BL} \rightarrow N_1 N_1) \times 2 BR(N_1 \rightarrow e^+ W^-)^4 \times \mathcal{L} \\
\approx 100 \text{ fb} \times \left( \frac{1}{3} \right) \times \left( \frac{1}{3} \right) \times 2 \left( \frac{3}{10} \right)^4 \times \left( \frac{6}{9} \right)^4 \times 100 \text{ fb}^{-1} \approx 4.
\]  

(19)

Where the \( BR(X_1 \rightarrow N_1 N_1) = 1/3 \) due to the three possible generations of right-handed neutrinos and \( BR(N_1 \rightarrow e^+ W^-) \approx 3/10 \) due to model specific parameters and kinematics, see [7] and the benchmark defined below. In order to make a realistic calculation of the number of events we pick a benchmark scenario:

Benchmark Scenario I: \( m_{A_{BL}} = 220 \text{ GeV}, m_{X_1} = 200 \text{ GeV}, m_{Z_{BL}} = 1 \text{ TeV}, \mu_{BL} = 150 \text{ GeV}, M_{BL} = 150 \text{ GeV}, m_{N_1} = 95 \text{ GeV}, \) for \( i = 1..3, m_{\tilde{\tau}_i} = 150 \text{ GeV}, m_{\tilde{e}_i} = 150 \text{ GeV} \) and all other sfermions at 1 TeV.

The sfermions masses effect the \( Z_{BL} \) width. In this case \( \sigma_{pp \rightarrow X_1 A_{BL}} = 65.7 \text{ fb}, \) and we display the predicted number of events in Table I for the five possible final states with an e and/or a \( \mu \). We also show the combinatorics factor which takes into account the branching ratios of the Higgses into right-handed neutrinos, right-handed neutrinos into leptons and Ws into jets. This number can be multiplied by any cross section and integrated luminosity to yield the number of events. In this case, if we ignore the displaced vertices, the main SM background is \( t \bar{t} W^\pm t \bar{t} W^\pm \) and it has a negligible cross section so that while there are only a few number of events, they are background free. This does not change the fact though that the reconstruction would be quite challenging due to the presence of eight jets in the final state. Imposing the condition that the invariant mass of two jets, \( |M(jj) - M_W| < 15 \text{ GeV} \), can improve the reconstruction process as well as the order millimeter displaced vertices due to the long lifetimes of the right-handed neutrinos.

In Model II the Higgs, \( S_1 \), can decay mainly into two sfermions. Here, for simplicity we focus on a scenario where the gravitino is the LSP with a simplified spectrum: \( m_{\tilde{G}} < m_{\tilde{N}_1} < m_{\tilde{\tau}_i}, m_{\tilde{e}_i}, m_{\tilde{\mu}_i} < m_{S_1}/2 \). This type of spectrum could be obtained in gauge mediation. Assuming that the neutralino is Bino-like, the pair production could lead to signals with multileptons, multijets and missing energy:

\[
pp \rightarrow S_1 A_S \rightarrow e^+ e^- S_1 e_i^+ e_i^- \rightarrow e^+ e^- e^\pm e^\mp e_i^+ e_i^- \gamma \gamma \gamma \gamma + E_T^{miss}
\]

In principle, these type of signals are quite spectacular because they could also include displaced vertices due to the lifetime of the neutralinos. Unfortunately, the branching ratio of the Higgs into sfermions is quite spectrum dependent. For a recent study of long-lived neutralinos see Ref. [8]. We postpone the study of these channels for a future publication.

Summary and Outlook: In this letter we have discussed how to test the mechanism responsible for the LSP stability at the LHC. We note that if \( R \)-parity is conserved dynamically, a Higgs boson which decays mainly into two right-handed neutrinos (“leptonic” Higgs) or into two sfermions is likely. In the first case one could have spectacular lepton number violating signals with four secondary vertices due to the existence of long-lived right-handed neutrinos. The second case could have peculiar signals with multileptons and multijets. A more detailed study will appear in a future publication [9]. These signals, together with the standard channels for the discovery of SUSY, could help us to establish the underlying theory at the TeV scale.

Acknowledgments: P.F.P. would like to thank Espresso Royale for hospitality. We would like to thank V. Barger and T. Han for discussions. This work is supported in part by the U.S. Department of Energy under grant No. DE-FG02-95ER40896, and by the Wisconsin Alumni Research Foundation.

| Final State | Combinatorics | Number of Events |
|-------------|---------------|-----------------|
| 4e± 8j     | 0.00072       | 4.8             |
| 3e± µ± 8 j | 0.0012        | 7.6             |
| 2e± 2µ± 8 j| 0.0015        | 9.7             |
| e± 3µ± 8 j | 0.00081       | 5.3             |
| 4µ± 8 j    | 0.00035       | 2.3             |

TABLE I: Number of events for the five possible four same-sign leptonic final states (with e or µ) for a luminosity of 100 fb\(^{-1}\) and a pair production cross section of 65.7 fb corresponding to benchmark I. We also display the combinatorics factor which combines the branching ratios for the Higgses into right-handed neutrinos, right-handed neutrinos to specific leptonic final states and Ws into jets.
[1] M. Drees, R. Godbole and P. Roy, *Theory and Phenomenology of Sparticles*, (World Scientific, 2004).

[2] R. Barbier et al., Phys. Rept. 420 (2005) 1.

[3] L. M. Krauss and F. Wilczek, Phys. Rev. Lett. 62 (1989) 1221; A. Font, L. E. Ibanez and F. Quevedo, Phys. Lett. B 228 (1989) 79; S. P. Martin, Phys. Rev. D 46 (1992) 2769.

[4] P. Fileviez Pérez and S. Spinner, Phys. Rev. D 83 (2011) 035004.

[5] K. Nakamura et al. [PDG Collaboration], J. Phys. G G37 (2010) 075021.

[6] P. Fileviez Perez, S. Spinner, M. K. Trenkel, [arXiv:1103.5504 [hep-ph]].

[7] P. Fileviez Pérez, T. Han and T. Li, Phys. Rev. D 80 (2009) 073015.

[8] P. Meade, M. Reece and D. Shih, JHEP 1010 (2010) 067.