Optimisation of Sensor Electrode Size for in Electrical Resistance Tomography Implementing Conducting Boundary Strategy

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Abstract. Electrical Resistance Tomography (ERT), due to its diverse advantages has become a promising technique for monitoring and analysing various industrial flows. In this research, an ERT system employing a conducting bubble column was studied because a majority of industrial processes use metal composites for their columns. This paper presents an approach to obtain the optimum size of electrodes in ERT to maximize the capability of an ERT system. A finite element model using COMSOL software was developed to investigate the effect of the electrode size in ERT on sensing field distribution. By adapting the conducting boundary strategies in COMSOL, wider and longer electrodes reduce the potential change near source, suggesting less current density near source. Besides that, wider and longer electrodes also reduce the potential drop and improve the signal strength in Electrical Resistance Tomography. The optimum size of 12 mm x 100 mm electrode is sufficient for the proposed ERT system using conducting bubble column.

1. Introduction
In recent years, the applications of tomographic techniques as a robust non-invasive tool for direct analysis of characteristics of multiphase flows are widely used. One of the applications is to investigate gas holdup distributions in a bubble column which has been the focus of many previous studies [1–10]. Tomography offers a unique opportunity to reveal the complexities of the internal structure of an object without having to invade it. One of the most extensive modalities of tomography is Electrical Resistance Tomography (ERT). ERT is an accepted diagnostic technique for imaging the
interior of opaque systems. It is relatively safe and inexpensive to operate besides being fast, thus enabling real-time monitoring of processes. This technique has been applied in many areas, including medical imaging, environmental monitoring, and industrial processes. There are many researches conducted on ERT. In developing the ERT system, it is vital to consider the sensor selection, which the sensor is the electrode in this research.

The parameters of electrode’s characteristic to be considered when adopting ERT are the materials used to construct the sensor, their shape and size, number, and position of the electrodes [11]. In ERT, the electrodes need to be in continuous contact with the fluid inside the vessel which differs from Electrical Capacitance Tomography (ECT). The main medium in contact with ERT sensors has to be conductive to allow injected current to pass through the medium [12]. ECT is used when continuous material such as air or oil does not conduct electricity, whereas for ERT, the continuous material (e.g. water, acids, bases and ionic solutions) is electrically conducting. The voltage measurement in ERT can only be obtained when the injected current finds its conductive pass [13].

This paper investigated and analysed the effect of varying electrode size on the potential distribution of ERT using conducting bubble columns. Modelling and simulation of the system was done by using COMSOL Multiphysics software (simulation software package for various physics and engineering applications).

2. Methodology
Before creating the model using COMSOL, it was decided that a flexible circuit board as the electrode would be used. It is to be noted that metal electrodes for electrically-conducting (metallic) column differ slightly from a non-conducting (insulating) column in which the electrodes need to be insulated from the conducting column. A design was proposed for the electrode fabrication to be implemented in ERT system deploying conducting vessel. Figure 1 and 2 show the design of electrode fabrication using flexible circuit board and an inner cross section view of the proposed system.

![Figure 1. Electrode Fabrication using flexible circuit board](image1)

![Figure 2. Inner Cross Section View](image2)
upcoming circuit since the loss in measurement sensitivity using larger electrodes is minimal [14]. The parameters used throughout the simulation are shown in Table 1. It is assumed that the electrodes make electrical contact with the fluid inside the column but do not affect the normal mass transfer within the system.

| Symbol                      | Quantity                      |
|-----------------------------|-------------------------------|
| Column Inner radius         | 50 mm                         |
| Column Outer radius         | 52.5 mm                       |
| Column Height               | 300 mm                        |
| Number of electrodes (N)    | 16                            |
| Electrode’s material        | Gold                          |
| Electrode’s height (h)      | 10 mm, 20 mm, ..., 110 mm, 120 mm |
| Electrode’s width (w)       | 3 mm, 6 mm, ..., 15 mm, 18 mm  |
| Current excitation          | 20 mA                         |
| $\sigma_{\text{water}}$    | $5 \times 10^{-3}$ S/m        |

Prior to building a model using COMSOL Multiphysics, users need to specify the desired space dimension, select physics interfaces and study type. A 3D space dimension, Electric Currents interface under the AC/DC branch and stationary study were selected respectively for the simulation study. After that, the following steps were taken:

i. Create a physical model using available geometries:
   A 3D physical model has been developed such that it mimics a real system. Sixteen electrodes that were insulated from the column wall were placed equidistantly inside the column.

ii. Define materials for each domain in the created model:
   The materials for each related domain in the model were defined such that it also resembles a real one. The column itself was defined as stainless steel material and the main medium inside the column was the water with a conductivity of 5 mS/m.

iii. Assign relevant physics interface and define boundary and initial conditions that describe real experiment setup:
   Electric Currents interface was chosen since it would produce an electrical field and has the electrical potential distribution required for the analysis. It also contained the equations, boundary conditions, and current sources for modelling electric currents in conductive media, solving the electric potential. By adopting the conducting boundary strategy, a constant current of 20 mA was applied at source electrode, $e_s$ and the output voltages from 15 pairs of electrodes from $e_1$ to $e_{15}$ were measured. Meanwhile, the column itself was grounded and acted as the current sink. The cross-section view of the 3D COMSOL Multiphysics model is in Figure 3.
iv. Mesh the model

In a simulation process, meshing geometry can be crucial in obtaining the best results in a faster way. Extra fine meshing under meshing physics-controlled setting is chosen since denser meshing would provide a more reliable finite element method (FEM) simulation. Figure 4 shows the meshed system under investigation.

Figure 4. Extra Fine Meshing using COMSOL

v. Run the study:

The investigated model is simulated using the default solver under stationary study. In applying the stationary solver, it is assumed that the load and deformation do not vary in time. All modelling formulations are based on Maxwell’s equation. The physic interface chosen earlier solves the current conservation equation for the electric potential.

To solve for varying length and width, a Parametric Sweep study node has been added to the study to perform parametric variation. Parametric Sweep study finds a solution to a sequence of PDE problems that arise the parameters of interest are varied. The parameters which are the electrode length and width in this case are globally defined in the model.

vi. Pre-process the data for result analysis

Last but not least, the results are pre-processed and analysed and were presented in the next section.

3. Results and Discussion

The simulation results of the ERT model using stainless steel pipe are presented in this section. In this study, the potential distributions produced by varying the size of the electrodes of a 20 mA current source were analysed. Firstly, the effects of varying electrode height, h for different electrode width, w
(5 mm, 10 mm, 12 mm) in a homogeneous solution were analysed. These are shown in Figure 5, 6 and 7. The potential profiles at each electrode excluding the source were plotted in Figure 5a, 6a and 7a correspondingly. As can be seen from Figure 5a, 6a, and 7a, different electrode heights produced different output values and the values are significantly larger for the electrodes near to the source. The output potential was significantly higher near the current injection electrodes and slightly smaller for the longer electrodes at other locations. For different electrode heights, electric potential at the nearest and furthest electrodes from source were observed in Figure 5b, 6b and 7b. From the simulations, it is found that the electric potential for e1 of 10 mm length is smaller than 20 mm length. According to the literature that had been done, it is believed that this is due to the equipotential averaging and electrode size trade off as been discussed in [14]. Ideally, a small surface area preferably a needle point is desired for voltage measurement. This is to avoid averaging several equipotential at that particular electrode. So, it is believed that, for 10 mm electrode length of e1, it did average several equipotential which made the output smaller than 20 mm length. As the length is increased, more equipotential were being averaged at the electrode surface. Starting from 20 mm length till 120 mm, it is noticed that the potentials difference between e1 and e8 slowly decreasing as the electrodes get longer. Electrodes with greater length reduced the potential near the excitation which is the result of less current density near the excitation electrode. In addition to that, based on Ohm’s Law and resistance equation, it is found that the output potential is inversely proportional with the surface area of the electrode in which the surface area includes the length and width of the electrode. When varying the electrode’s height for different electrode’s width, it is observed that the output potential reading especially the one near to the source electrode becomes higher as the width is increased. The effect of increasing the width is discussed thoroughly latter.

(a) Potential profiles around the electrodes
(b) Potential at electrodes 1 and 8

Figure 5. Effect of Varying Electrode Height for 5 mm Electrode Width

(a) Potential profiles around the electrodes
(b) Potential at electrodes 1 and 8

Figure 6. Effect of Varying Electrode Height for 10 mm Electrode Width
Electrodes with greater axial length would slow the attenuation of the sensing field around the centre plane where the electrode’s centre is located. In addition, the sensing field would have better uniformity and space distribution of the sensing field was expanded [15]. Increasing the electrode height would improve the evenness of the sensing field as shown in Figure 8. The potential distributions in the figure obtained from COMSOL are for the electrodes with height of 30 mm, 60 mm and 100 mm.

By choosing an electrode height that equals 100 mm, the effects of varying electrode width, $w$ of 3 mm, 6 mm, 9 mm, 12 mm and 18 mm on potential distribution were simulated and analysed. Figure 9a shows the potential distribution for the homogeneous systems of each width mentioned earlier. Meanwhile, Figure 9b shows the potential between the nearest and furthest electrode from the source, $e_s$. 
As can be seen, the electric potential of the electrodes especially the one near to the source produce higher output as the width increased. In addition to that, the potential difference for the electrode nearest, e1 and furthest, e8 from the source also becomes greater when the width is wider. This is due to the higher current densities of the wider electrodes. From the results in Figure 9, it is concluded that wider electrodes improve the signal strength of the system which will also improve the ability of object detection.

To illustrate the potential distributions for different electrode widths obtained in COMSOL Multiphysics, the xy-plane of the results are presented in Figure 10. Wider electrodes provide a more uniform current distribution in the region of interest. In addition to that, it improves the evenness of the field distribution resulting in improved signal strength. However, narrower electrodes must be used when a higher number of electrodes are placed around the circumference to avoid shunting where the current bypasses the medium and goes around the circumference [16].

The sensitivity of the electrode width on anomaly detection was examined further using a spherical inclusion (inclusion diameter $D=10$ mm). The inclusion is the phantom of bubble. A sensor sensitivity indicates how much the sensor output changes when the measured quantity changes. Sensors that measure very small changes must have very high sensitivity. Figure 11 shows the potential change $\Delta V/V_h$ with respect to the corresponding potential measured in the homogenous medium induced by the spherical inclusion. The positive potential differences for electrodes near to the source (e1, e2, e3, e13, e14 and e15) were in response of the higher current densities near source electrode, e_s. The potential difference corresponding to the homogeneous medium drops to a negative value for e4 to e12 as the current densities deteriorate as it travels through the medium. Overall, the responses became more sensitive when the electrode width is bigger and it was observed that 12 mm electrode width is the most sensitive towards the inclusion. The sensitivity became lower for electrode width of 15 mm and above possibly due to the shunting effect mentioned earlier.
4. Conclusion
An electrode size needs to be identified before setting up the final hardware of an ERT system. Ideally, the injection electrode should be as large as possible while the measuring electrodes should be as small as possible. The size related trade-off has to be considered since the electrodes are alternately used for injection and measurement electrodes. It is suggested that electrode size of 12 mm x 100 mm is good and sufficient for the ERT system using metal wall. Results from the simulation clearly show that wider and longer electrodes reduce the potential change near source, suggesting less current density near source. Besides that, wider and longer electrodes also reduce the potential drop and improve the signal strength in ERT. The numerical method has proven that the optimum electrode width should cover 60% of the sensing surface and electrodes with greater height produce better axial field distribution. Normally, improving the evenness of the current distribution always counteract the shunting effect of the system. By taking into account the effects of varying electrode sizes, the electrode width must be carefully selected to prevent the shunting effects in ERT. Last but not least, it is to be state that the electrode size of 12 mm x 100 mm has been applied to the conducting bubble column successfully in the experiment.

5. References
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