First Observation of Directed Flow of Hypernuclei $^3\Lambda H$ and $^4\Lambda H$ in $\sqrt{s_{NN}} = 3$ GeV

Au+Au Collisions at RHIC

The STAR Collaboration

We report here the first observation of directed flow ($v_1$) of the hypernuclei $^3\Lambda H$ and $^4\Lambda H$ in mid-central Au+Au collisions at $\sqrt{s_{NN}} = 3$ GeV at RHIC. These data are taken as part of the beam energy scan program carried out by the STAR experiment. From 165 million good events in 5-40% centrality, about 8400 $^3\Lambda H$ and 5200 $^4\Lambda H$ candidates are reconstructed through two- and three-body decay channels. We observe that these hypernuclei exhibit significant directed flow. Comparing to that of light nuclei, it is found that the mid-rapidity $v_1$ slopes of $^3\Lambda H$ and $^4\Lambda H$ follow baryon number scaling, implying that the coalescence is the dominant mechanism for these hypernuclei production in such collisions.

When a nucleon is replaced by a hyperon (e.g., $\Lambda$, $\Sigma$) with strangeness $S = -1$, a nucleus is transformed into a hypernucleus which allows for the study of the hyperon-nucleon ($Y-N$) interaction. It is well known that two-body $Y-N$ and three-body $Y-N-N$ interactions, especially at high baryon density, are essential for understanding the inner structure of compact stars [1, 2]. A new result on $\Lambda - p$ elastic scattering with better precision has been reported by Jefferson Lab [3], which may help constrain the neutron star equation of state. Until recently, almost all hypernuclei measurements have been carried out with light particle (e.g., $e$, $\pi^\pm$, $K^\mp$) induced reactions [4, 5], where spectroscopic properties of hypernuclei are analyzed around the saturation density.

Utilizing hypernuclei production in heavy-ion collisions to study the $Y-N$ interaction and the properties of QCD matter has been a subject of interest in the past decades [6–10]. However, due to limited statistics, measurements have been mainly focused on the light hypernuclei lifetime, binding energy and production yields [9, 11, 12]. Thermal model [13] and hadronic transport model with coalescence afterburner [14, 15] calculations have predicted abundant production of light hypernuclei in high-energy nuclear collisions, especially at high baryon density. Anisotropic flow has been commonly used for studying the properties of matter created in high energy nuclear collisions. Due to its genuine sensitivity to early collision dynamics [16–19], the first order coefficient of the Fourier-expansion of the azimuthal distribution in the momentum space, $v_1$, also called the directed flow, has been analyzed for many particle species ranging from $\pi$-mesons to light nuclei [20–25]. Collective flow is driven by pressure gradients created in such collisions. Hence, measurements of hypernuclei collectivity make it possible to study the $Y-N$ interactions in the QCD equation of state at high baryon density.

In this paper, we report the first observation of directed flow, $v_1$, of $^3\Lambda H$ and $^4\Lambda H$ in center-of-mass energy $\sqrt{s_{NN}} = 3$ GeV Au+Au collisions. The data were collected by the STAR experiment at RHIC with the fixed-target (FXT) setup in 2018. A gold beam of energy 3.85 GeV/u is bombarded on a gold target of thickness 1% interaction length, located at the entrance of STAR’s Time-Projection Chamber (TPC) [26]. The TPC, which is the main tracking detector in STAR, is 4.2 m long and 4 m in diameter, positioned inside a 0.5 T solenoidal magnetic field along the beam direction. The collision vertex position of each event along the beam direction, $V_z$, is required to be within ±2 cm of the target position. An additional requirement on the collision vertex position to be within a radius $r$ of less than 2 cm is imposed to eliminate background events from interactions with the beam pipe. Beam-Beam Counters (BBC) [27] and the Time of Flight (TOF) detector [28] are used to obtain the minimum bias (MB) trigger condition. After event selection, a total of $2.6 \times 10^8$ MB events are used for further analysis.

The centrality is determined using the charged particle multiplicity distribution within the pseudo-rapidity region $-2 < \eta < 0$ together with Monte Carlo (MC) Glauber calculations [29, 30]. The directed flow ($v_1$) is measured with respect to the first-order event plane, determined by the Event Plane Detector (EPD) [31] which covers $-5.3 < \eta < -2.6$ for the FXT setup. For this analysis, a relatively wide centrality range, 5-40%, is selected where both the event plane resolution and the hypernuclei yield are maximized. The event plane resolution in the centrality range is 40−75% [32]. Detailed information on the event plane resolution can be found in the Supplemental Material.

In order to ensure high track quality, we require that the number of TPC points used in the track fitting (nHitsFit) to be larger than 15 (out of a maximum of 45). $^3\Lambda H$ is reconstructed via both two-body and three-body decays $^3\Lambda H \rightarrow ^3He + \pi^-$ and $^3\Lambda H \rightarrow d + p + \pi^-$ while $^4\Lambda H$ is reconstructed via the two-body decay channel $^4\Lambda H \rightarrow ^4He + \pi^-$. Charged particles, including $\pi^-$, $\rho$, $d$, $^3He$ and $^4He$ are selected based on the ionization energy loss $(dE/dx)$ measured in the TPC as a function of rigidity $(p/q)$, where $p$ and $q$ are the momentum and charge of the particle. The secondary decay topology is reconstructed using the KFParticle package based on a Kalman filter method [33]. The package also utilizes the covariance matrix of reconstructed tracks to construct a
set of topological variables. Selection cuts on these variables are placed on hypernuclei candidates to enhance the signal significance. Figure 1 shows the reconstructed invariant mass distributions for $\Lambda$, $^3\Lambda$H, and $^4\Lambda$H, which are reconstructed using various decay channels in the corresponding transverse momentum $p_T$ - rapidity $y$ regions as listed in Table I. Combinatorial background is estimated by rotating decay particles through a random angle between 10 and 350 degrees. For the $\Lambda$, the $\pi^-$ is rotated. For the $^3\Lambda$H two-body decay, the $^3\Lambda$H is rotated, and for the $^4\Lambda$H three-body decay, the deuteron is rotated. The combinatorial background, shown as the shaded region, is normalized in the invariant mass region: (1.14, 1.16), (3.01, 3.04), and (3.95, 4.0) GeV/$c^2$ for $\Lambda$, $^3\Lambda$H and $^4\Lambda$H, respectively. Background-subtracted invariant mass distribution (filled circles) in each panel are fitted with a linear function plus a Gaussian distribution to extract the signal counts.

![FIG. 1. Reconstructed $\Lambda$ hyperon and hypernuclei invariant mass distributions from $\sqrt{s_{NN}} = 3$ GeV Au+Au collisions in the corresponding $p_T$ - $y$ regions listed in Table I. While top panels are for $\Lambda \to p + \pi^-$ and $^3\Lambda$H $\to ^3\text{He} + \pi^-$, bottom panels represent the hypertriton two-body decay $^3\Lambda$H $\to ^3\text{He} + \pi^-$ and three-body decay $^4\Lambda$H $\to d + p + \pi^-$, respectively. Combinatorial backgrounds, shown as histograms, are constructed by rotating decay daughter particles. Background-subtracted invariant mass distributions are shown as filled circles.](image)

![FIG. 2. A hyperon and hypernuclei acceptance, shown in $p_T$ versus $y$, from the $\sqrt{s_{NN}} = 3$ GeV Au+Au collisions. Dashed rectangular boxes illustrate the acceptance regions used for directed flow analysis, and the red arrow in panel a) represents the target rapidity ($y_{\text{target}} = -0.045$).](image)

Figure 2 shows the $p_T$ versus $y$ acceptance of the reconstructed $\Lambda$, $^3\Lambda$H and $^4\Lambda$H candidates in the center-of-mass frame. Following the established convention [34], the negative sign is assigned to $v_1$ in the rapidity region of $-1.05 < y < 0$. The $p_T$-y acceptance windows used for our analysis are tabulated in Table I and also indicated in Fig. 2.

For $p_T$-integrated $v_1$ measurements, the $p_T$-dependent reconstruction efficiency needs to be accounted for, which is estimated by the embedding method in STAR analyses [9, 35]. Monte-Carlo generated hyperons and hypernuclei are passed through the GEANT3 simulation of the STAR detector. The simulated TPC response is then embedded into data, and the whole event is processed and analyzed using the same procedure as in the data analysis. The two-dimensional reconstruction efficiency, including the detector acceptance, in $p_T$-$y$ are obtained for each decay channel, and applied to candidates in the data accordingly [36]. Kinematically, the three-body decay of $^4\Lambda$H is very similar to the background of correlated $d + \Lambda$ due to the very small $\Lambda$ separation energy of $^4\Lambda$H. Such correlated $d + \Lambda$ pairs that pass the $^4\Lambda$H three-body decay topological cuts are subtracted statistically (For details, see Fig. 3 in the Supplemental Material). The $^4\Lambda$H signal fraction within the invariant mass window (2.988, 2.998) GeV/$c^2$ and rapidity range (-1.0, 0.0) is estimated to be $0.69 \pm 0.03$.

The directed flow of $\Lambda$, $^3\Lambda$H and $^4\Lambda$H are extracted with the event plane method [37]. In each rapidity bin, the azimuthal angle with respect to the reconstructed event plane ($\Phi = \Phi' - \Psi_1$) is further divided into four equal bins with a width of $\pi/4$, where $\Phi'$ and $\Psi_1$ are the azimuth

**TABLE I. $p_T$-$y$ acceptance windows of light nuclei, $\Lambda$ hyperon and hypernuclei used for directed flow analysis.**

| Mass Number (A) | Particle | $p_T$ (GeV/$c$) | $y$ |
|----------------|----------|----------------|-----|
| 1              | $\Lambda, p$ | (0.4, 0.8)     | (-1.0, 0.0) |
| 2              | $d$      | (0.8, 1.6)     | (-1.0, 0.0) |
| 3              | $^3\Lambda$H | (1.0, 2.5)     | (-1.0, 0.0) |
| 4              | $^3\Lambda$H | (1.2, 2.4)     | (-1.0, -0.1) |
| 5              | $^4\Lambda$H | (1.2, 3.0)     | (-1.0, -0.2) |

The directed flow of $\Lambda$, $^3\Lambda$H and $^4\Lambda$H are extracted with the event plane method [37]. In each rapidity bin, the azimuthal angle with respect to the reconstructed event plane ($\Phi = \Phi' - \Psi_1$) is further divided into four equal bins with a width of $\pi/4$, where $\Phi'$ and $\Psi_1$ are the azimuthal
angle of a particle candidate and the first order event plane, respectively. After applying the reconstruction efficiency correction, the azimuthal angle distributions are fitted with a function $f(\Phi) = c_0 + 2v_1^{obs}\cos(\Phi) + 2v_2^{obs}\cos(2\Phi)$, where $c_0$, $v_1^{obs}$ and $v_2^{obs}$ are fitting parameters, and correspond to the normalization constant, the observed directed and the elliptic flow, respectively. To obtain the final $v_1$ in a wide centrality range of 5-40% centrality in this analysis, the observed directed flow $v_1^{obs}$ needs to be corrected for the average event plane resolution $(1/R)$ [37], i.e. $v_1 = v_1^{obs} \cdot (1/R)$, and $(1/R) = \sum_i (N_i/R_i)/\sum_i N_i$, where $N_i$ and $R_i$ stand for the number of particle candidates and the first order event plane resolution in the $i$-th centrality bin, respectively.

The resulting $\Lambda$ hyperon and hypernuclei $v_1(y)$, from 5-40% mid-central Au+Au collisions at $\sqrt{s_{NN}} = 3$ GeV, are shown in Fig. 3. For comparison, the $v_1(y)$ of $p$, $d$, $t$, $^3$He and $^4$He from the same data [32] are shown as open symbols. $v_1(y)$ of $\Lambda$, $p$, $d$, $t$, $^3$He and $^4$He are fitted with a third-order polynomial function $v_1(y) = a \cdot y + b \cdot y^2 + c \cdot y^3$ in the rapidity ranges listed in Table I, where $a$, $b$, $c$ stands for the mid-rapidity slope $dv_1/dy|_{y=0}$, and $a$, $b$, $c$ are fitting parameters. Due to limited statistics, the hypernuclei $v_1(y)$ distributions are fitted with a linear function $v_1(y) = a \cdot y$, in the rapidity range $-1.0 < y < 0.0$. The linear terms for light nuclei are plotted as dashed lines in the positive rapidity region, while for $\Lambda$, $^3$H and $^4$H, they are shown by the yellow-red lines in the corresponding panels. The $\Lambda$ result is close to that of the proton, and hypernuclei $v_1(y)$ distributions are also similar to those light nuclei with the same mass numbers. This is the first observation of significant hypernuclei directed flow in high-energy nuclear collisions.

Systematic uncertainties are estimated by varying track selection criteria for particle identification, as well as cuts on the topological variables used in the KFParticle package [33]. Major contributors to the systematic uncertainty are listed in Table II. As one can see, the dominant sources of systematic uncertainty are from hypernuclei candidate selection, estimated by varying topological cuts and nHitsFit. Event plane resolution determination also contributes 1.4% [36]. Assuming these sources are uncorrelated, the total systematic uncertainty is obtained by adding them together quadratically.

| Source                  | $^3$H   | $^4$H   |
|-------------------------|---------|---------|
| Topological cuts        | 1.3%    | 9.4%    | 8.0%    |
| nHitsFit                | 9.0%    | <1.0%   |
| EP Resolution           | 1.4%    | 1.4%    |
| Total                   | 13.1%   | 8.3%    |

TABLE II. Sources of systematic uncertainties for mid-rapidity slope $dv_1/dy|_{y=0}$ of $^3$H and $^4$H.

The results of the mid-rapidity slope $dv_1/dy$ for $\Lambda$, $^3$H (both two- and three-body decays) and $^4$H are shown in Fig. 4, as filled squares, as a function of particle mass. For comparison, $v_1$ slopes of $p$, $d$, $t$, $^3$He and $^4$He from the same 5-40% $\sqrt{s_{NN}} = 3$ GeV Au+Au collisions are shown as open circles. The $\Lambda$ hyperon and hypernuclei slopes $dv_1/dy$ are all systematically lower than the nuclei of same mass numbers. Linear fits $(f = a + b \cdot mass)$ are performed on the mass dependence of $dv_1/dy$ for both light nuclei and hypernuclei. For light nuclei, only statistical uncertainties are used in the fit, while statistical and systematic uncertainties are used for hypernuclei. The slope parameters $b$ are $0.3323 \pm 0.0003$ for light nuclei and $0.27 \pm 0.04$ for hypernuclei. As one can see, their slopes are similar within uncertainties.

Using transport models JAM [19, 38] and UrQMD [18], $v_1(y)$ of $\Lambda$ and hypernuclei are simulated for the $\sqrt{s_{NN}} = 3$ GeV Au+Au collisions within the same centrality and kinematic acceptance used in data analysis. For comparison, similar calculations are performed for light nuclei. The simulation is done in two steps: (i) using the JAM model (with momentum-dependent potential) and UrQMD model (without momentum-dependent potential) in the mean field mode with the incompressibility $\kappa = 380$ MeV to produce neutrons, protons and $\Lambda$s at kinetic freeze-out; (ii) forming hypernuclei through the coalescence of $\Lambda$ and nucleons, similar to the light nuclei production with the coalescence procedure discussed in [32]. The probability for hypernuclei production is...
dictated by coalescence parameters of relative momenta $\Delta p < 0.12 (0.3) \text{ GeV}/c$ and relative distance $\Delta r < 4 \text{ fm}$ in the rest frame of $nn\Lambda$ ($nnp\Lambda$) for $^3_{\Lambda}H$($^4_{\Lambda}H$). These parameters are chosen such that the hypernuclei yields at mid-rapidity can be described [9]. The rapidity dependences of $v_1$ from the model calculations are then fitted with a third-order polynomial function within the rapidity interval $-1.0 \leq y \leq 0.0$. The resulting mid-rapidity slopes are shown in Fig. 4 as red and blue bars for JAM and UrQMD models, respectively. In the figure, results for light nuclei from JAM are also presented as gold bars.

Both transport models (JAM and UrQMD) plus coalescence afterburner calculations for hypernuclei are in agreement with data within uncertainties. Interactions among baryons and strange baryons are important ingredients in the transport models, especially in the high baryon density region [39, 40]. The properties of the medium is determined by such interactions. In addition, the yields of hypernuclei, if created via the coalescence process, are also strongly affected by the hyperon and nucleon interactions. In our treatment, the coalescence parameters used ($\Delta r, \Delta p$) reflect the production probability determined by $N-N$ and $Y-N$ interactions [15, 41, 42]. The mass dependence of the $v_1$ ($y$) slope implies that coalescence might be the dominant mechanism for hypernuclei production in such heavy-ion collisions. The mass dependence of the hypernuclei $v_1$ slope also seems to be similar to that of light nuclei, as shown in Fig. 4, although it may not necessarily be so due to the differences in $N-N$ and $Y-N$ interactions. Clearly, precision data on hypernuclei collectivity will yield invaluable insights on $Y-N$ interactions at high baryon density.

This is the first report of the collectivity of hypernuclei in heavy-ion collisions. Hydrodynamically, collective motion is driven by pressure gradients created in such collisions. This work opens up a new direction for studying $Y-N$ interaction under finite pressure [43]. This is important for making connection between nuclear collisions and the equation of state which governs the inner structure of compact stars.

To summarize, we report the first observation of hypernuclei $^3_{\Lambda}H$ and $^4_{\Lambda}H$ $v_1$ from $\sqrt{s_{\text{NN}}} = 3 \text{ GeV}$ mid-central 5-40% Au+Au collisions at RHIC. The rapidity dependences of their $v_1$ are compared with those of $\Lambda, p, d, t, ^3He$ and $^4He$ in the same collisions. It is found that, within uncertainties, the mass dependent $v_1$ slope of hypernuclei, $^3_{\Lambda}H$ and $^4_{\Lambda}H$ is similar to that of light nuclei, implying that they follow the baryon mass scaling. Calculations from transport models (JAM and UrQMD) plus coalescence afterburner can qualitatively reproduce the rapidity dependence of $v_1$ and the mass dependence of $v_1$ slope. These observations suggest that coalescence of nucleons and hyperon $\Lambda$ could be the dominant mechanism for the hypernuclei $^3_{\Lambda}H$ and $^4_{\Lambda}H$ production in such collisions.

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Supplemental Material: First Observation of Directed Flow of hypernuclei $^{3}_ΛH$ and $^{4}_ΛH$ in $\sqrt{s_{NN}} = 3$ GeV Au+Au Collisions at RHIC

The STAR Collaboration

I. EVENT PLANE RESOLUTION

In this measurement, the directed flow is calculated via the event-plane method [1]. For each event, the event plane is reconstructed using the Event Plane Detector (EPD) [2]. For the estimation of the resolution for the first-order event plane, please refer to [3] for details. Figure 1 shows the first-order event plane resolution (Top) and the distributions of raw yields for $^{3}_ΛH$ 2-body decay and $^{4}_ΛH$ as a function of collision centrality (Bottom). Events from centrality 5-40% (shown by the black dashed lines) are selected for analysis to optimize the signal.

![Event Plane Resolution](image)

**FIG. 1:** Top: First-order event plane resolution as a function of collision centrality. Bottom: Distribution of raw yields as a function of collision centrality for $^{3}_ΛH$ 2-body decay and $^{4}_ΛH$.

II. TOPOLOGICAL CUTS USED FOR $Λ$, $^{3}_ΛH$, AND $^{4}_ΛH$.

Table I shows topological variables cuts employed for $Λ$, $^{3}_ΛH$, and $^{4}_ΛH$ candidate selection. Their definitions are: (1) nHitsFit is the number of TPC points used in the track fitting; (2) $l$ is the decay length from primary vertex to decay vertex; (3) $l_{dl}$ is the distance from the decay point of the candidate to the primary vertex normalized on the error; (4) $\chi^2_{topo}$ is the mother particle’s $\chi^2$ deviation from the primary vertex; (5) $\chi^2_{ndf}$ is the $\chi^2$ deviation between daughter particles; (6) $\chi^2_{prim}$ defines the daughter particle’s $\chi^2$ deviation from the primary vertex.
III. FITTING AZIMUTHAL DISTRIBUTIONS FOR HYPERNUCLEI

Figure 2 shows the distributions of $dN/d(\phi - \Psi_1)$ as a function of $\phi - \Psi_1$ for $^3\Lambda H$ 2-body and 3-body decay and $^4\Lambda H$ in different rapidity regions, for centrality bin 5-40%. Distributions of $dN/d(\phi - \Psi_1)$ is fitted by $dN/d(\phi - \Psi_1) = p_0(1 + 2v_1^{obs}\cos(\phi - \Psi_1) + 2v_2^{obs}\cos(2(\phi - \Psi_1)))$, where $p_0$, $v_1^{obs}$ and $v_2^{obs}$ are normalization parameter, observed directed and elliptic flows, respectively. In each panel, red lines show the fitting results, which can well describe data points.

![Figure 2](image-url)

**FIG. 2:** In 3 GeV Au+Au collisions, the angular distributions of $^3\Lambda H$ 2-body and 3-body decays and $^4\Lambda H$ in different rapidity regions.

IV. PURITY FOR THE $^3\Lambda H \rightarrow p + d + \pi^-$ 3-BODY DECAY

The kinematically correlated $\Lambda$ and deuteron would form a peak around $M(\Lambda) + M(d) = 2.9913$ GeV/c when $C(k^*) > 1$ at $k^* \rightarrow 0$, where $C(k^*)$ is the kinematic correlation function of $\Lambda$ and deuteron and $k^*$ is relative momentum between $\Lambda$ and deuteron. These correlated $\Lambda + d$ pairs would coincide with the reconstructed $^3\Lambda H$ signals via $^3\Lambda H \rightarrow p + d + \pi^-$ channel even after combinatorial background subtraction, since $^3\Lambda H$ is weakly bounded with a small $\Lambda$ separate energy $B_\Lambda \sim 0.13 - 0.41$ MeV/c$^2$ [4] and the finite experimental momentum resolution could not
separate the $^3\Lambda H$ invariant mass peak from the correlated $\Lambda + d$ peak.

Although the invariant masses of correlated $\Lambda + d$ background and the real signal are close, some of their topological kinematics are different. For correlated $\Lambda + d$ background, the decay daughters of $\Lambda \rightarrow p\pi^-$ and deuteron come from different vertices, while the daughters of $^3\Lambda H$ are all produced at the same vertex. $\chi_{NDF}^2$ is a topological variable calculated by KFParticle package [5] that characterizes whether particle trajectories intersect at the same vertex within uncertainties. A cut on $\chi_{NDF}^2$ can greatly suppress the correlated background. However, these correlated background cannot be fully rejected by such a cut, since $\Lambda$ daughters and the deuteron could be very close at $k^* \rightarrow 0$ and they cannot be distinguished experimentally due to the finite spatial resolution. Therefore, the template fitting method is used to extract the fraction of $^3\Lambda H$ signal in the reconstructed sample. $\chi_{NDF}^2$ distributions of the candidate $^3\Lambda H$ in the data are extracted and then fitted with the template $\chi_{NDF}^2$ distributions of correlated background and pure signal. The $^3\Lambda H$ candidates from data are selected within $M(^3\Lambda H) \pm 2\sigma$ with all topological cuts used in the analysis applied expect for the $\chi_{NDF}^2$ cut. The combinatorial background is estimated by rotating decay daughter particles. The templates for $^3\Lambda H$ signals are obtained from embedding simulated Monte Carlo (MC) $^3\Lambda H$ signal into real data and applying the same reconstruction procedure as in data analysis. Similarly, correlated background templates are built by embedding simulated $\Lambda$ particles into real data and pairing MC $\Lambda$ with deuteron tracks from real data. MC $\Lambda$ are weighted according to the measured $\Lambda$ spectra. The reconstructed $\Lambda + d$ from embedding are weighted with kinematic correlation functions [6] and applied with the same topological and invariant mass selection cuts as data samples. The $\chi_{NDF}^2$ distribution of reconstructed $^3\Lambda H$ candidates are fitted with $f_{data} = p_0 \cdot (p_1 \cdot f_{^3\Lambda H} + f_{Ad})$, where $f_{data}$, $f_{^3\Lambda H}$ and $f_{Ad}$ refer to the normalized $\chi_{NDF}^2$ distributions of $H3L$ candidates from real data, $H3L$ and $\Lambda + d$ templates from embedding, respectively. The parameter $p_0$ and $p_1$ are fitting parameters. The $^3\Lambda H$ purity, $p_{^3\Lambda H}$, is defined as the fraction of $^3\Lambda H$ signal in the reconstructed $^3\Lambda H$ candidates with all topological cuts applied in the data analysis. Figure 3 shows the estimated $p_{^3\Lambda H}$ as a function of rapidity. The $^3\Lambda H$ yield is calculated as $p_{^3\Lambda H} \cdot N^{raw}$, where $N^{raw}$ is the raw $^3\Lambda H$ candidate counts.

![Purity vs Rapidity](image)

FIG. 3: The estimated purity of $^3\Lambda H p_{^3\Lambda H}$ in the reconstructed $^3\Lambda H$ candidate sample via $^3\Lambda H \rightarrow p + d + \pi^-$ as a function of rapidity.

V. MODEL ANALYSIS AND COMPARISON

A. Determine the coalescence parameters from measured hypernuclei $dN/dydydp_T$

Transport models JAM and UrQMD are utilized to generate nucleons and $\Lambda$ hyperons at 3 GeV. As these models can not reproduce light nuclei and hypernuclei yields [7, 8], a simple coalescence approach is employed to form light nuclei and hypernuclei using spatial and momentum distributions of nucleons and $\Lambda$ hyperons at a time of 50 fm/$c$ in the medium evolution. For a hypernucleus, it forms in two steps. Firstly, a light nucleus core is formed based on the relative momentum $\Delta p$ and relative distance $\Delta r$ of constituent nucleons in their rest frame. Then the light nucleus core combines with a $\Lambda$ to form a hypernucleus following a similar process. The coalescence parameters, $\Delta p$ and $\Delta r$,
are determined by matching the $dN/ptdy$ spectrum from the calculations to the corresponding experimental data for a given light nucleus or hypernucleus [9]. The $\Delta p$ is 0.3 GeV/c for both deuteron and triton, and $\Delta r$ is 4.5 fm and 4 fm for them, respectively. The $\Delta r$ is 4 fm for both $^3\Lambda H$ (deuteron + $\Lambda$) and $^4\Lambda H$ (triton + $\Lambda$), and $\Delta p$ is 0.12 GeV/c and 0.3 GeV/c, respectively. In the model, we assume that the branching ratios are 25% and 50% for $^3\Lambda H \rightarrow ^3\Lambda H + ^3\Lambda H \rightarrow ^3\Lambda H + ^3\Lambda H$ and $^4\Lambda H \rightarrow ^4\Lambda H + ^4\Lambda H$, respectively. These results from JAM plus coalescence calculations can qualitatively reproduce the $^4\Lambda H$ and $^3\Lambda H$ spectra [9], as shown in Fig. 4.

![Graph of $^3\Lambda H$ and $^4\Lambda H$ pT spectra](image)

**FIG. 4:** $^3\Lambda H$ and $^4\Lambda H$ pT spectra in three different rapidity intervals from 0-10% central Au+Au collisions at $\sqrt{s_{NN}} = 3$ GeV. Only the statistical uncertainties are plotted. The dashed lines are results from JAM plus coalescence calculations. For model results, spectra are scaled with the branching ratios which are assumed to be 25% and 50% for $^3\Lambda H \rightarrow ^3\Lambda H + ^3\Lambda H$ and $^4\Lambda H \rightarrow ^4\Lambda H + ^4\Lambda H$, respectively [9].

**B. $v_1(y)$ distributions from JAM and UrQMD model calculations**

Figure 5 shows the $\Lambda$ hyperon and hypernuclei directed flow $v_1$, as a function of rapidity, from the $\sqrt{s_{NN}} = 3$ GeV 5-40% mid-central Au + Au collisions. The results of a linear fit:

$$v_1(y) = v_1^s y$$

for $^3\Lambda H$ and $^4\Lambda H$ are shown as red-yellow lines in the figure. The range of $(-1.0 < y < 0)$ is used for $v_1$ measurements of all light nuclei, $\Lambda$ hyperon and hypernuclei, as well as their model results. As the $\Lambda$ and light nuclei have an obvious non-linear tendency at $y < -0.5$. So a 1st plus 3rd order polynomial function

$$v_1(y) = v_1^s y + p_1 y^3$$

is used to fit them. The same fitting procedure is applied to model calculations, as well as to the $^3\Lambda H$ and $^4\Lambda H$ model calculations. While for the $v_1$ results from $^3\Lambda H$ and $^4\Lambda H$, due to the limitation of their statistics, we use the 1st order polynomial function to describe them. In Fig. 5, transport model calculations (fit results) from JAM and UrQMD are shown as cross circles and cross squares (long dashed and dot-dashed lines), respectively. The resulting mid-rapidity $v_1$ slopes for all the particles under study are summarized in Fig. 4 of the manuscript.
The directed flow $v_1$, shown as a function of rapidity, from the $\sqrt{s_{NN}} = 3$ GeV 5-40% mid-central Au + Au collisions. In case of $^3_\Lambda$H $v_1$, both results from 2-body (circles) and 3-body (triangles) decays are shown. The fitted linear terms for light nuclei are plotted as dashed lines in the positive rapidity region, while for $\Lambda$ hyperon, $^3_\Lambda$H and $^4_\Lambda$H, they are shown by the yellow-red lines in the corresponding panels. The rapidity dependence of $v_1$ for $p$, $d$, $t$, $^3$He, and $^4$He are also shown as open markers, including circles, diamonds, up-triangles, down-triangles and squares, respectively. The corresponding $v_1$ results extracted from 1st+3rd order polynomial fits, within $-1.0 < y < 0$, are shown as dashed lines in the positive rapidity region. Transport model calculations (fit results) from JAM and UrQMD are shown as cross circles and cross squares (long dashed and dot-dashed lines), respectively.
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