Exergetic Investigation of the Effects of Superheating and Subcooling on Performance of a Vapor Compression Refrigeration Cycle

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Abstract
The aim of this study is to investigate the effects of superheating and subcooling values on the cooling performance of a vapor compression refrigeration cycle. For this purpose, a refrigeration cycle with cooling capacity of 8 kW using R404A was examined by changing superheating and subcooling values. Energy, exergy and entropy balances were applied for evaporation and condensation temperatures of 0°C and 45°C, respectively. The coefficient of cooling performance (COP), the amount of energy transfer, rate of exergy destruction and rational exergy efficiency of each components (evaporator, compressor, condenser and expansion valve) and the whole system were determined. The compressor work, coefficient of performance and second law efficiency increased by 0.7%, 1.61% and 1.56%, respectively, per one-degree increment of superheating in the evaporator.

Keywords: Exergy, Exergy destruction, Refrigeration cycle, Superheating, Subcooling.

1. INTRODUCTION
Simple vapor compression refrigeration system is generally preferred for refrigeration and air conditioning systems. The refrigerant leaves from evaporator and enters compressor as a saturated vapor. Also, in the condenser unit, the refrigerant is completely condensed to saturated liquid [1]. In practice, however, the refrigerant enters the compressor as superheated vapor and enters the throttle valve as compressed liquid. Thus, for design of a vapor compression refrigeration system, the refrigerant in the exit of the condenser and evaporator are often considered as subcooled and superheated, respectively [2]. And superheating and subcooling procedures are applied to improve performance of the refrigeration system [3].

Bilgili et. al. (2017) performed thermodynamic analysis of an inter-city bus air conditioner using R600 as working fluid. Superheating and subcooling temperature values defined as 10 °C for exergy efficiency and exergy destructions of the bus air conditioning system [4]. Yılmaz and Aktaş (2019) investigated ejector refrigeration (ER) system using exhaust waste heat of a heavy vehicle engine using R134a and R245fa. In order to determine the performance coefficient, engineering equation solver software was used and subcooling and superheating were taken as 1 °C [5].

Beşer and Mobedi (1999) analyzed the effect of subcooling the refrigerant at the exit of the condenser in a simple vapor compression cycle on the energetic performance for different refrigerants, such as R407C, R134a and R22 [6]. Kızılkan et. al. (2006) examined subcooling and superheating heat exchangers of vapor compressed refrigeration system for R22 and R407c. The optimum areas of subcooling and superheating heat exchangers determined in relation to economics and working performance [7]. Yan et. al. (2019) theoretically evaluated a novel vapor compression refrigeration cycle with subcooler for freezer applications to increase cooling effect and the COP of the system [8].

Different applications of the refrigeration cycle have widely examined in literature. Chen et. al. (2019) integrated solar absorption-subcooling cycle to vapor compression refrigeration cycle to enhance the cooling capacity [9]. Bellos and Tzivanidis (2019) compared transcritical CO2 refrigeration systems to conventional system. And COP enhancement of the configuration which contain mechanical subcooling was 75.8% compared to without subcooling cycle [10]. Wang and Zhang (2019) modeled parametrically simple transcritical refrigeration cycles using R744 as refrigerant with different subcooling methods. They applied energy, exergy and economic analyses to the models with different subcooling methods in order to investigate the effect of the ambient
temperature on the performance [11].

In the literature, it was widely mentioned that subcooling of the refrigerant at the condenser outlet improved the performance. However, it was not stated that in which range of the subcooling value increases the system performance. Besides, the effect of the superheating at the evaporator outlet on cooling performance was not investigated in literature. In the present study, energy and exergy analyses were applied to a vapor compression refrigeration cycle working with R404A. The main purpose of this paper is to emphasize the importance of the effect of the subcooling and superheating on the system performance. Thus, besides energy transfer rate and exergy destruction rate within the all components and entire cycle, COP of cycle for cooling and rational exergy efficiency of all components and whole cycle were determined from energy and exergy analyses.

3. THERMODYNAMICS ANALYSIS

To calculate the energy transfer rate, exergy destruction rate, the entropy generation rate and the exergy efficiency of each components of the refrigeration cycle, energy and exergy balances were applied to the cycle. In the calculations, the following assumptions were made:

- All processes in the cycle are assumed as steady state and no frictional loss throughout the cycle.
- The change of kinetic and potential energies of the entire system are zero and there are no chemical, magnetic and nuclear reactions.
- Heat transfer takes place only in the condenser and the evaporator units so the compression and expansion processes are adiabatic.
- The work transfer in the expansion valve is neglected.
- The mechanical and electrical efficiency of the compressor are taken as 70% and 75%, respectively.
- Evaporation and condensation processes occur at a constant pressure.

Energy balance can be defined as the difference between inlet and outlet energy transfer rate by heat, work and mass equals to the net energy change in total energy of the system [12, 13].

\[ \dot{E}_{\text{heat,in}} + \dot{E}_{\text{mass,in}} - \dot{E}_{\text{work,out}} = \Delta \dot{E}_{\text{system}} \]  

(1)

This equation is also called as the first law of thermodynamics or the energy conservation law. From this equation, rate of heat transfers in the evaporator and the condenser units and work transfer in the compressor unit are determined. Since the rate of removing heat from cold medium or the evaporator capacity is known, the refrigerant mass flowrate can be determined as follow.

\[ m_r = \dot{Q}_e / (h_1 - h_4) \]  

(2)

Following equation was used to define the isentropic efficiency of the compressor [14].

\[ \eta_i = 0.874 - 0.0135 P_c / P_e \]  

(3)

By the definition of the isentropic efficiency of the compressor, enthalpy of the compressor outlet is obtained.

\[ h_2 = h_1 + \frac{(h_2i - h_1)}{\eta_i} \]  

(4)

where \( h_2i \) is the enthalpy at the outlet of the condenser in the case of isentropic compression process. The COP for cooling is the heat removing from refrigerated space divided by required work.

\[ \text{COP} = \frac{\dot{Q}_e}{W_{elc}} = h_3 - h_4 \cdot \eta_{mec} \cdot \eta_{elc} \]  

(5)
The exergy destruction rate equals to exergy rate by net mass input, net heat input and net work output [15].

\[
\dot{X}_{\text{dest}} = \dot{X}_{\text{mass,in}} + \dot{X}_{\text{heat,in}} - \dot{X}_{\text{work,out}} \tag{6}
\]

The flow exergy is evaluated as [15]:

\[
\varepsilon = (h - h_0) - T_0(s - s_0) \tag{7}
\]

The general exergy destruction rate is

\[
\dot{X}_{\text{dest}} = \dot{m}(\varepsilon_{\text{in}} - \varepsilon_{\text{out}}) + \left(1 - \frac{T_0}{T_0}\right)\dot{Q}_{\text{in}} - \dot{W}_{\text{out}} \tag{8}
\]

The second law or exergy efficiency

\[
\eta_{\text{II}} = \frac{\text{COP}}{\text{COP}_{\text{Carnot}}} \tag{9}
\]

The rational exergy is taken [13].

\[
\psi = \frac{\dot{X}_{\text{dest, out}}}{\dot{X}_{\text{comp,in}}} \tag{10}
\]

The rate of energy transfers, the rate of exergy destruction and the rational exergy efficiency equations are summarized in Table 2. The dead state properties are taken at the temperature of 10°C and pressure of 101.3 kPa.

### Table 2. The equations of the energy transfer rate, exergy destruction rate and the exergy efficiency

| Component       | Energy transfer rate | Exergy destruction rate | Exergy efficiency |
|-----------------|----------------------|-------------------------|-------------------|
| Evaporator      | \( \dot{Q} = m_c(h_{x2} - h_{x4}) \) | \( \dot{X} = m_c(\varepsilon_{x2} - \varepsilon_{x4}) + \left(1 - \frac{T_0}{T_0}\right)\dot{Q}_c \) | \( \psi = \frac{\dot{X}}{\dot{Q}_c} \) |
| Compressor      | \( \dot{W}_{\text{comp,in}} = m_c(h_{x5} - h_{x4}) \) | \( \dot{X}_{\text{comp,in}} = m_c(\varepsilon_{x5} - \varepsilon_{x4}) + \dot{W}_{\text{comp}} \) | \( \psi_{\text{comp}} = \frac{\dot{X}_{\text{comp,in}}}{\dot{W}_{\text{comp}}} \) |
| Expansion valve | \( h_3 = h_4 \) | \( \dot{X}_{\text{exp}} = m_c(h_{x4} - h_{x5}) \) | \( \psi_{\text{exp}} = \frac{\dot{X}_{\text{exp}}}{\dot{X}_{\text{comp,in}}} \) |
| Condenser       | \( \dot{Q} = m_c(h_{x2} - h_{x4}) \) | \( \dot{X} = m_c(\varepsilon_{x2} - \varepsilon_{x4}) + \left(1 - \frac{T_0}{T_0}\right)\dot{Q}_c \) | \( \psi = \frac{\dot{X}}{\dot{Q}_c} \) |
| Refrigeration cycle | \( \dot{Q} + \dot{W}_{\text{comp,in}} - \dot{Q} = 0 \) | \( \dot{X} = \left(1 - \frac{T_0}{T_0}\right)\dot{Q} + \dot{W}_{\text{comp}} + \dot{X}_{\text{exp}} - \dot{X}_{\text{comp,in}} \) | \( \psi = \frac{\dot{X}}{\dot{Q}} \) |

### 4. RESULTS AND DISCUSSIONS

The energy and exergy analyses results of refrigeration cycle using R404A at the superheating and subcooling values of and are summarized in Table 3. In this conditions, the exergy efficiency of entire system and the COP for cooling were obtained as 35.1% and 3.81, respectively. Besides, the maximum and minimum exergy destructions were recorded in the expansion valve as 0.43 kW and in the evaporator unit as 8.62 W, respectively.

COP for cooling increased by increasing the superheating and subcooling values, for instance COP at lowest and highest superheating and subcooling values were computed as 1.787 and 2.038, respectively. Effects of superheating and subcooling on the coefficient of cooling performance is shown in Figure 2. According to graphs, the effect of subcooling in improvement of COP is more significant to superheating.

**Figure 2. Variations of COP for cooling with superheating and subcooling values.**

The exergy destruction in whole cycle was low at the smallest superheating and at the highest subcooling values. Effects of superheating and subcooling on the exergy destruction in the refrigeration cycle is plotted in Figure 3. The minimum and maximum exergy destruction in cycle were obtained as 2971.0 W at \( sh=1^\circ\text{C}, sc=9^\circ\text{C} \) and 3263.1 W at \( sh=8^\circ\text{C}, sc=1^\circ\text{C} \) respectively.

In the compressor, the amount of exergy destructions at \( sh=1^\circ\text{C} \) and at \( sh=8^\circ\text{C} \) were 360.26 W and 371.33 W, respectively. There was no change in the exergy destruction in compressor for different subcooling values. In addition, effects of superheating and subcooling on the exergy destruction in evaporator, condenser and expansion valve are illustrated in Figure 4, 5 and 6, respectively.

### Table 3. The energy and exergy analyses results at and

| Location | (°C) | (kPa) | (kg/s) | (kJ/kg) | (kJ/kgK) | (kJ/kg) | (kW) |
|----------|------|-------|--------|---------|----------|---------|------|
| 0 | 10 | 101.3 | – | 237.2 | 1.02525 | 0 |
| 1 | 5 | 604 | 0.0826 | 223.1 | 0.83197 | 40.66 | 3.3584 |
| 2 | 58.8 | 2063 | 0.0826 | 253.2 | 0.84765 | 66.30 | 5.4754 |
| 3 | 37 | 2063 | 0.0826 | 108.4 | 0.39337 | 50.17 | 4.1433 |
| 4 | 0 | 604 | 0.0826 | 108.4 | 0.41174 | 44.97 | 3.7138 |

| Component | Energy transfer rate | Exergy destruction rate | Exergy efficiency |
|-----------|----------------------|-------------------------|-------------------|
| Evaporator | 9.472 kW | 360.26 W | 35.1% |
| Compressor | 2.484 kW | 66.30 W | 85.2% |
| Expansion valve | – | 66.30 W | 89.6% |
| Condenser | 11.956 kW | 16.92 W | 98.7% |
| Refrigeration cycle | – | 3069 W | 35.1% |
The exergy destruction in evaporator increased when superheating decreased and subcooling increased. The minimum exergy destruction in the evaporator was computed at $\text{sh}=1$ and it increased from 0.454 W to 3.237 W when the superheating increased from 1°C to 9°C. Otherwise, the exergy destruction in condenser increased when superheating increased and subcooling decreased. The minimum exergy destruction in the condenser was obtained at $\text{sc}=12$ and it decreased from 16.05 W to 1.239 W when the superheating increased from 1°C to 9°C. In the expansion valve exergy destruction was dependent on subcooling and as subcooling value increases from 1°C to 9°C, exergy destruction has decreased from 557.4 W to 413.0 W.

Figure 7 indicates the effect of the superheating and subcooling on the rational exergy efficiency of evaporator. As shown in this figure, when the subcooling values increased, the rational exergy efficiency of evaporator decreased linearly from 96.85% to 96.43% at $\text{sh}=9$ and when the superheating values increased, rational exergy efficiency increased from 96.85% to 99.86% at $\text{sc}=1$.
Also, Figure 8 illustrates the effects of the superheating and subcooling on the rational exergy efficiency of condenser. According to this figure, the rational exergy efficiency of condenser decreased by the superheating value from 98.65% to 96.85% at and increased by the subcooling value from 98.65% to 99.90% at .

Further, the effects of the superheating and subcooling on the rational exergy efficiency of expansion valve is shown in Figure 9. Variations in subcooling value caused a significant change in the rational exergy efficiency of expansion valve. For example, the rational exergy increased from 86.84% to 90.00%. On the other hand, variations in superheating value didn’t cause any change.

Furthermore, variation of the rational exergy efficiency of refrigeration cycle with the superheating and subcooling is presented in Figure 10. As can be seen in this figure, the effect of the subcooling on the exergy efficiency of whole cycle was more considerable than the effect of the superheating. For instance, the exergy efficiency linearly increased with subcooling value from 31.98% to 35.38% at , otherwise, the exergy efficiency linearly increased with superheating value from 31.98% to 32.42% at .

5. CONCLUSIONS
The superheating and the subcooling values were increased 1°C to 8°C and 9°C, respectively under the same evaporation and condensation pressures. The effect of the superheating and the subcooling values on the performance of a refrigeration system using R404A is investigated.

The following main results are achieved from this study:

a) The compression work or the electrical consumption rate increased approximately 0.7% per 1° increment in superheating and %5 for 8° difference in superheating. In contrast, there has been no change in the rate of compression work for different subcooling values.

b) The COP increased by an average of 1.61 and 1.54, respectively, with a one-degree increase in superheating and subcooling.

c) The change in exergy destruction in the compressor was negligible for increase in superheating and subcooling values. The change in exergy destruction in entire system decreased by 1.03% and 1.06%, respectively, per one-degree increment of superheating and subcooling.

d) Exergy efficiency increased by approximately 1.56% for each one-degree increase in both superheating and subcooling.

6. NOMENCLATURE

$\dot{E}$ : Energy transfer rate (kW)

$h$ : Specific enthalpy (kJ/kg)

$m$ : Mass flow rate (kg/s)

$P$ : Absolute pressure (kPa)

$\dot{Q}$ : Heat transfer rate (kW)

$s$ : Specific entropy (kJ/kgK)
6.1. Greek symbols

\( \eta \) : Efficiency (\%)

\( \mu \) : Dynamic viscosity of fluid (kg/m/s)

\( \psi \) : Rational exergy efficiency (\%)

\( \Delta \) : Difference

6.2. Subscripts

0 : Dead state

1, 2, … : Cycle locations

II : Second law

com : Compressor

c : Condenser or condensation

cons : Consumed

dest : Destroyed

e : Evaporator or evaporation

elc : Electrical

exp : Expansion valve

f : Saturated liquid phase

g : Saturated vapor phase

gen : Generation

in : Inlet

mec : Mechanical

rc : Refrigeration cycle

sc : Subcooling

sh : Superheating

out : Outlet

Abbreviations

COP : Coefficient of performance

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