Hidden SU(N) Glueball Dark Matter

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We investigate the possibility that the dark matter candidate is from a pure non-abelian gauge theory of the hidden sector, motivated in large part by its elegance and simplicity. The dark matter is the lightest bound state made of the confined gauge fields, the hidden glueball. We point out this simple setup is capable of providing rich and novel phenomena in the dark sector, especially in the parameter space of large \(N\). They include self-interacting and warm dark matter scenarios, Bose-Einstein condensation leading to massive dark stars possibly millions of times heavier than our sun giving rise to gravitational lensing effects, and indirect detections through higher dimensional operators as well as interesting collider signatures.

**Introduction.** An outstanding issue of fundamental importance in particle physics is the nature of the dark matter (DM). This question is particularly intriguing and perplexing, given the preponderance of DM over visible matter and its profound gravitational effects throughout the evolution of the universe.

In this work, we like to investigate the viability of the dark matter candidate from the hidden sector with a non-abelian gauge symmetry, a minimal theory with non-trivial mass scale. The gauge group is chosen to be \(SU(N)\), and, for simplicity, neither fermions nor any other particle is introduced in that sector. The dark matter is the lightest hidden glueball state, which is likely a scalar field, and a non-perturbative bound state made of a pair of confined gauge fields. This is a very simple setup with only a handful of parameters, which are the intrinsic scale \(\Lambda\), the number of colors \(N\), and \(\theta\) — for the T and P-odd \(\theta\)-term in the hidden sector. They control the mass and all the couplings of the hidden glueball dark matter (GDM), named \(\phi\) hereafter.

In spite of the simplicity of this setup, we will show that the hidden glueball indeed satisfies all the conditions for a dark matter candidate. Moreover, such a dark matter could be both self-interacting and warm, thus safely evading all the potential problems of the usual collisionless cold dark matter. The scalar GDM could have the novel feature of Bose-Einstein condensation into compact objects thus plausibly leading to interesting gravitational effects such as microlensing. It could also be tested in particle physics experiments if there exist interactions of it with standard model particles via higher dimensional operators. We will elaborate on these points in order in the following sections \([1]\).

**Hidden Glueball as Dark Matter.** In this work, we consider dark matter candidate (DMC) from a very simple setup, a hidden sector non-abelian gauge symmetry with only gauge fields and without fermions. The Lagrangian of the model is

\[
\mathcal{L} = -\frac{1}{4} H^a_{\mu \nu} H^{a \mu \nu}.
\]

where \(H^a_{\mu \nu}\) is the gauge field strength of the group \(SU(N)\), with an unspecified value of \(N\) to be determined later. As is well known the gauge coupling \(g_h\) becomes large at low energy scale and dimensional transmutation generates a scale \(\Lambda\) for the theory, similar to the emergence of the QCD scale. Around the scale \(\Lambda\), the physical degrees of freedom turn into a tower of hidden glueballs. From the knowledge based on existing calculations, the lowest lying glueball states when \(\theta = 0\) carry quantum numbers \(J^{PC} = 0^{++}\), or \(0^{-+}\) \([6, 7]\). Their masses depend on the two parameters of the theory, \(\Lambda\) and \(N\). Also from lattice calculations \([8, 9]\), the lightest glueball masses approach a constant at large \(N\), and can be parametrized as \(m = (\alpha + \beta/N^2)\Lambda\) where \(\alpha, \beta\) are order one parameters. In general, we could also introduce the \(\theta\)-term in the above Lagrangian, which is \(C\) even and \(P\) odd. It can mix the \(0^{++}\) and \(0^{-+}\) states and lightest glueball state is then not an eigenstate under \(P\).

We argue that within this simple setup the lightest hidden glueball state \(\phi\) could be a candidate for dark matter \([10]\). It could be cosmologically long lived. As the lightest state, there is nothing in the hidden sector that \(\phi\) could decay into. It is possible for \(\phi\) to decay into two gravitons, and this decay rate can be estimated as \(\Gamma_{\phi} \sim m^5/M_{pl}^4 \tau_v^{-3} (m/10^7 \text{GeV})^3\), where \(\tau_v = 10^{17}\text{ sec}\) is the age of our universe. The lifetime of \(\phi\) against gravitational decay can be long enough if its mass is less than \(10^7\text{ GeV}\). Moreover, the hidden glueball \(\phi\) particles could have the correct relic density and be (non-)relativistic enough as will be elaborated in the next section. So far, we have not written down any interactions between the hidden section and the visible sector, which by gauge invariance is only possible in the form of higher dimensional operators. We will explore the resulting experimental bounds in an example where the hidden GDM \(\phi\) decays into photons.

**Self-interacting Dark Matter.** The effective potential of a real scalar \(\phi\) takes the form

\[
V(\phi) = \frac{1}{2} m^2 \phi^2 + \frac{1}{3!} \lambda_3 \phi^3 + \frac{1}{4!} \lambda_4 \phi^4 + \frac{1}{5!} \lambda_5 \phi^5 + \cdots \, .
\]
where the \( \cdots \) represent higher power terms. It is useful to consider the large \( N \) behavior of these couplings,

\[
\lambda_3 = \frac{\kappa_3 m}{N}, \quad \lambda_4 = \frac{\kappa_4}{N^2}, \quad \lambda_5 = \frac{\kappa_5}{mN^3},
\]

where \( \kappa_{3,4,5} \) are order one parameters to be determined from non-perturbative calculations. From these interactions, we could obtain the \( 3 \to 2 \) elastic scattering cross section of \( \phi \) as a function of the two model parameters, \( m(\Lambda) \) and \( N \), \( \sigma_{3\to2} \sim 1/(m^2 N^3) \). The self-interacting dark matter scenario has been proposed \([11]\) to reconcile the core/cusp problem in dwarf galaxy observations and simulations. For this scenario to work, the elastic scattering cross section of dark matter must lie in the range 0.1 cm\(^2\)/gram \(< \sigma_{3\to2}/m < 10 \) cm\(^2\)/gram. This requirement puts a correlated constraint on \( m \) and \( N \),

\[
m \sim 0.1 \text{ GeV} \cdot N^{-4/3}.
\]

This region is shown between the blue curves in Fig. 1

**Self Heating and Warm Dark Matter.** In addition to elastic scattering, the effective interactions in [(2)] also allow \( \phi \) to have the inelastic \( 3 \leftrightarrow 2 \) annihilation, which changes the \( \phi \) particle number. The analog of cross section could be estimated as \( \sigma_{3\to2} \sim 1/(m^2 N^6) \). The \( 3 \to 2 \) reaction rate is given by \( \Gamma_{3\to2} = n_{\phi}^2 \sigma_{3\to2} \), where \( n_{\phi} \) is the \( \phi \) number density in the universe. This interaction could play an important role on the velocity dispersion of dark matter in the early universe, because after each \( 3 \to 2 \) reaction the two outgoing \( \phi \) particles are relativistic. If this process has a larger reaction rate than the Hubble expansion, the annihilation will keep heating up the \( \phi \) particles until it reaches the balance with the inverse process where two energetic \( \phi \) ‘s annihilate into three. In this model, there are no interactions for \( \phi \) and SM particles to exchange heat in equilibrium [(12)], the entropy of the \( \phi \) particles is conserved, \( \frac{dS}{da}(\rho_{\phi} + p_{\phi} a^3/T) = 0 \). For non-relativistic \( \phi \) ‘s, i.e., \( T_{\phi} \ll m \), one could derive

\[
T_{\phi}(a) \approx T_{\phi}(a_0) \left( 1 + \frac{3T_{\phi}(a_0)}{m} \ln \frac{a}{a_0} \right)^{-1},
\]

where \( a \) is the Hubble radius at given time in the early universe \( (a = 1 \) today), and \( a_0 \) \(< a \) corresponds to an earlier time. This means the \( \phi \) particles thermalize to a temperature which drops more slowly than \( 1/(\ln a) \) with the expansion of the universe, as first noted in [(13)]. In contrast, the temperature of the photons falls as \( T_{\gamma} \sim 1/a \), leading to the interesting possibility that the hidden and SM sectors have their own temperatures and evolve separately.

It is useful to expand the energy density and pressure of \( \phi \) to next order in \( T_{\phi}/m, \rho_{\phi} = mn_{\phi}(1 + 3T_{\phi}/(2m)), \ p_{\phi} = mn_{\phi}T_{\phi}/m \). With this one can obtain the evolution equation of \( n_{\phi} \) as a function of \( a \),

\[
\frac{d(n_{\phi} a^3)}{da} \approx - \frac{(n_{\phi} a^3)}{a} \frac{3 T_{\phi}}{m}.
\]

The message here is that the number density of \( \phi \) dilutes faster than \( a^{-3} \), thus the total number of \( \phi \) is still decreasing while the \( 3 \to 2 \) annihilation is in equilibrium. The consumption of \( \phi \)’s is used to maintain the temperature of the remaining \( \phi \) particles. The final DM relic density is given by \( n_{\phi} \) at the decoupling of \( 3 \to 2 \) annihilation. In Fig. 2 we show the ratio of the decoupling temperature \( T_{\phi}^{\gamma} \) to the mass of \( \phi \) that is needed to give the correct dark matter relic density, for different values of the photon temperature at this epoch [(15)].

Before the \( 3 \to 2 \) decoupling, the temperature \( T_{\phi} \) stays roughly one order of magnitude below the mass \( m \). The strongly coupled \( \phi \) particles form a fluid with a large speed of sound \( c_s = \sqrt{2T_{\phi}/(3m)} \sim 0.3c \). It allows the perturbations to the density of \( \phi \) within one Hubble patch to be smoothed out efficiently via collisional damping, thus offering the opportunity for \( \phi \) to be a warm DMC.

To find when the \( 3 \to 2 \) process decouples, or the corresponding temperature of photon \( T_{\phi}^{\gamma} \), we first express \( 3 \to 2 \) rate in terms of the photon temperature, \( \Gamma_{3\to2} = n_{\phi}^2 \sigma_{3\to2} \sim 10^{-17} \text{GeV}^2 T_{\phi}^5/(m^2 N^6) \). When it is equal to the Hubble rate, we get the photon temperature at \( 3 \to 2 \) decoupling \( T_{\phi}^{\gamma} \sim 1 \text{ keV} \left[ m/(1 \text{ keV}) \right]^{7/4} \left[ N/(10^4) \right]^{3/2} \). The collisional damping length scale (measured today) is determined by the Hubble radius at the \( 3 \to 2 \) decoupling

\[
R_{\text{cd}} = \frac{1}{H(T_{\phi}^{\gamma})} \frac{T_{\phi}^{\gamma}}{2.7 \text{ K}} \approx 0.1 \text{ Mpc} \left( \frac{1 \text{ keV}}{T_{\phi}^{\gamma}} \right).
\]

After the \( 3 \to 2 \) decoupling, the temperature of \( \phi \) will drop as \( 1/a^2 \) such that the velocity redshifts as \( 1/a \). We calculate the free streaming length of \( \phi \) particles from this time, \( T_{\phi}^{\gamma} \), to the time of matter-radiation equality,
The mass range of the boson star depends on whether the self-interaction of $\phi$ is repulsive or attractive. The size of the boson star is typically much larger than the inverse of the glueball mass. In the hidden glueball model Eq. (2), at low momentum transfer the effective coupling of the $\phi^4$ self interaction is

$$\lambda_{\text{eff}} = \lambda_3^2/(2m^4) + \lambda_4 = (\nu_3^2/2 + \kappa_4)/N^2 .$$  

Non-perturbative calculations are needed to reliably determine the size and signs of $\kappa_3, \kappa_4$, and in turn the fate of the condensate.

The opportunity to observe the microlensing effect arises if there is repulsive self interactions for the $\phi$ field, with $\lambda_{\text{eff}} > 0$. In this case, it has been calculated [18] that the boson star mass from condensation lies in the range $10^{-6}M_\odot$, for the glueball dark matter with mass from GeV to 0.1 keV scale. In particular, in the interesting window of Fig. [4] where the dark matter is both self-interacting and warm, the corresponding boson star mass is between $10^{-4} - 10^{-3}M_\odot$. On the other hand, if $\lambda_{\text{eff}} < 0$, the boson star mass would be too small to have an observable effect.

**Interactions with the SM Through Higher Dimensional Operators.** In general, there may exist interactions between the hidden sector and the SM sector. This may allow the glueball dark matter to be discovered through means other than gravitational effects. However, we do not want to introduce other particles just to facilitate these interactions, since as explained before, we want to explore how far our set up with just a simple pure $SU(N)$ gauge theory can go in addressing the DM issue. So, without introducing additional particles, gauge invariance dictates that these interactions may arise via higher dimensional operators, $\mathcal{L}_{\text{int}} = (1/M^n)H^\mu\nu\Pi_{\mu\nu}O_{SM}$, where $M$ is the cutoff scale. There are many choices for the $O_{SM}$ part. Here we discuss one representative which couples the hidden sector directly to photons

$$\mathcal{L}_{\text{int}} = \frac{1}{M^4}H^\mu\nu H^{\rho\sigma} (F_{\alpha\beta}F^{\alpha\beta}) \rightarrow \frac{N m^3}{M^4} \phi F_{\alpha\beta}F^{\alpha\beta} ,$$  

where $F$ is the photon field strength. In the second step, we go to the low scale where $\phi$ is the lightest glueball field. In the following, we choose the value of $N$ making $\phi$ a self-interacting dark matter, $N \approx \text{Max} [(m/0.1\text{GeV})^{-3/4}, 2]$. It is also worth noting that the effective interaction of $\phi$ is proportional to powers of its mass $m^3$.

From Eq. (9), the decay rate of $\phi$ into two photons is

$$\Gamma_{\phi \rightarrow \gamma\gamma} = \frac{N^2 m^9}{4\pi M^8} .$$  

There are experimental searches for monochromatic photon from decaying dark matter, from cosmic gamma rays to X rays and even extragalactic background lights [21–25]. They give the strongest constraints on the scale $M$.
for the dark matter \( \phi \) mass above \( \sim 100 \text{ keV} \). We show these constraints in Fig. [3].

For lower \( \phi \) masses, we find the energy loss constraints of stars place a stronger lower limit. The relevant reaction is the Primakoff type process \( e + \gamma \rightarrow e + \phi \). The cross section was calculated in [26].

\[
\sigma v = 64\pi \alpha \frac{\omega \Gamma_{\phi \rightarrow \gamma \gamma}}{m^2} \frac{(\omega^2 - m^2)^{1/2}(\omega - m)}{(m^2 - 2\omega m)^2},
\]

where \( \omega \) is the energy of the incoming photon and \( m \) is the mass of glueball dark matter. To calculate the rate of energy loss from the star via \( \phi \) emission, we first average the \( \sigma v \cdot \omega \) over the thermal photon energy distribution, and then the energy loss rate per unit volume is given by \( \Phi = n_e n_\gamma \langle \sigma v \omega \rangle \). We consider the energy loss argument [27] of horizontal branch stars (HB) and the cooling of type-II supernova (SN). For HB, the core temperature is \( 10 \text{ keV} \), the mass density is \( 10^5 \text{ g/cm}^3 \), and the energy loss rate per unit volume is required to be \( \Phi < 10^{-42} \text{ MeV}^5/\text{cm}^3 \). For SN, the core temperature is \( 30 \text{ MeV} \), both photon and electrons are thermalized, and the energy loss rate is required to be \( \Phi < 10^{-14} \text{ MeV}^5/\text{cm}^3 \). Their constraints on \( M \) (lower bound) is shown in Fig. [3].

Not-too-much energy loss of HB sets the strongest lower bound on \( M \) for \( \phi \) mass below \( \sim 100 \text{ keV} \). For the model to be realistic in cosmology, the hidden sector must not thermalize with the SM sector, at least not since the onset of BBN. We find this to be a subdominant constraint (shown by the blue curve in Fig. [3]).

The operators in Eq. [9] not only lead the glueball dark matter particle to decay, but also allows it to scatter with SM particles by virtue of the expansion \( H_{\mu\nu}H^{\mu\nu} \sim Nm^2\phi^2 + m^2\phi^2 + \cdots \). Given the above lower bounds on the cutoff scale \( M \), we find the direct detection cross section for the glueball dark matter is more than ten orders of magnitude below the current LUX bound [28]. This is consistent with the null results so far in the direct detections. It also implies that if the future direct detection experiments discovers the dark matter, it cannot originate from our dark matter candidate [29].

From Fig. [3] we find that for the dark matter mass \( m \) in the range \( \text{keV} \) to \( \text{MeV} \), the cutoff \( M \) is allowed to be as low as the weak (or TeV) scale. The effective operator in Eq. [9] could be generated by integrating out a heavy particle \( X \) in the ultraviolet theory, which carries both electromagnetic charge and color under the hidden \( SU(N) \) gauge group. If a pair of \( X \bar{X} \) can be produced at colliders, they would eventually form a heavy \( X \)-onium bound state and annihilate away into the hidden glueball dark matter or photons. The final states will exhibit exotic signatures like the quirks [30, 31].

Furthermore, if the heavy \( X \) particle is a fermion and also carries color under the \( SU(3)_c \) of QCD, the effective Lagrangian will contain an operator \( (1/M^4)(H\bar{H})(G\bar{G}) \) (similar to Eq. (12) of Ref. [32]). In the presence of the \( \theta H\bar{H} \) term from the hidden \( SU(N) \) theory, it induces an effective \( \theta_{QCD}GG \) term, with \( \theta_{QCD} \sim (m/M)^4 \), and makes a contribution to the neutron electric dipole moment (nEDM). The important point we want to make here is that nEDM bound does not require the \( \theta \) parameter of \( SU(N) \) to be unnaturally small, unlike \( \theta_{QCD} \). The current experimental upper bound on nEDM of around \( 10^{-26} \text{ cm} \) [33] translates, by the arguments of [34], into \( \theta_{QCD} \lesssim 10^{-13} \). From the above relation between \( \theta_{QCD} \) and \( \theta \), we find that \( \theta \) is allowed to be order one if \( m/M \lesssim 10^{-3} \), which is always satisfied from Fig. [3].

**Summary.** In this paper, we investigate the physics of \( SU(N) \) glueball dark matter from a pure gauge theory non-abelian hidden sector. In spite of the simple setup, with few parameters, there are quite a few novel features of this dark matter candidate. We have discussed the conditions for it to be self-interacting and/or warm dark matter. The glueball dark matter could also condense into more compact objects like boson stars and be observed by gravitational lensing effects. Therefore, our model can naturally accommodate the fact that there is only gravitational evidence for dark matter so far [35, 36]. It could also interact with the standard model sector via higher dimensional operators and subject to traditional direct searches for light scalar dark particles. The direct detection cross section of the glueball dark matter is constrained to be well below the experimental sensitivity, now as well as for the foreseeable future. We also comment on the possible UV origin of the higher dimensional operators leading to interesting collider signatures.

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We are aware of several other works which study dark matter with a non-abelian dark sector, however, these works involve in addition rather elaborate other intricacies with significantly different phenomenology from this study; see, e.g. [2–5].

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A positive direct detection signal would imply our hidden glueball dark matter cannot comprise all the dark matter relic density. There might be other components of dark matter.

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