NUSTAR OBSERVATIONS OF G11.2-0.3.

K. K. Madsen\textsuperscript{1}, C. L. Fryer\textsuperscript{2}, B. W. Grefenstette\textsuperscript{1}, L. A. Lopez\textsuperscript{3}, S. Reynolds\textsuperscript{4}, A. Zoglauer\textsuperscript{5}

\textsuperscript{1} Cahill Center for Astronomy and Astrophysics, California Institute of Technology, Pasadena, CA 91125, USA
\textsuperscript{2} LCS-2, Los Alamos National Laboratory, Los Alamos, NM 87545, USA
\textsuperscript{3} The Ohio State University, Columbus, OH 43210, USA
\textsuperscript{4} Physics Department, NC State University, Raleigh, NC 27695, USA
\textsuperscript{5} Space Sciences Laboratory, University of California, Berkeley, CA 94720, USA

\textit{Draft version March 3, 2020}

\textbf{ABSTRACT}

We present in this paper the hard X-ray view of the pulsar wind nebula in G11.2-0.3 and its central pulsar PSR J1811-1925 as seen by \textit{NuSTAR}. We complement the data with \textit{Chandra} for a more complete picture and confirm the existence of a hard, power-law component in the shell with photon index $\Gamma = 2.1 \pm 0.1$, which we attribute to synchrotron emission. Our imaging observations of the shell show a slightly smaller radius at higher energies, consistent with \textit{Chandra} results, and we find shrinkage as a function of increased energy along the jet direction, indicating that the electron outflow in the PWN may be simpler than that seen in other young PWNe. Combining \textit{NuSTAR} with \textit{INTEGRAL}, we find that the pulsar spectrum can be fit by a power-law with $\Gamma = 1.32 \pm 0.07$ up to 300 keV without evidence of curvature.

\textit{Subject headings: X-rays: individual (PSR J1811-1925), individual (G11.2-0.3)}

1. INTRODUCTION

According to conventional ideas, the young remnant of a core-collapse supernova (CCSN) ought to consist of a shell emitting brightly in radio synchrotron emission and thermal X-rays, containing a pulsar and pulsar-wind nebula (PWN). The Galactic pulsar birthrate (of order 1 – 2 per century; Vranjesic et al. 2004), in combination with standard estimates of the Galactic CCSN rate of 2 – 3 per century (e.g., Tammann et al. 1994) requires that a large fraction of CCSNe should produce pulsars, and any self-respecting pulsar ought to inflate a bright synchrotron nebula. Furthermore, something like 80\% of supernovae should be CCSNe (Tammann et al. 1994). The remnants of recent supernovae in our Galaxy fail significantly to live up to this expectation. The well-documented historical or quasi-historical supernovae of the past two millennia include five (likely) Type Ia SNe: G1.9+0.2 (ca. 1900 CE; Reynolds et al. 2008), Kepler (SN 1604), Tycho (SN 1572), SN 1006, and RCW 86 (SN 185; Williams et al. 2011), and two atypical CCSN remnants: Cas A, with a central non-pulsing neutron star (Pavlov et al. 2000), and the Crab, whose absence of any kind of external shell is a continuing embarrassment (unless the “shell” is emission at the edge of the synchrotron nebula; Hester 2008).

However, several other Galactic remnants are clearly quite young, though without as clear age documentation. The youngest of all known CCSN remnants containing a PWN is Kes 75 (G29.7−0.3), with an age estimated from expansion of 480 ± 50 years (Reynolds et al. 2018a). It has a very asymmetric partial shell surrounding a bright PWN. The next youngest, once associated with a claimed historical SN in 386 AD, but now known to suffer too much extinction to have been a naked-eye supernova, is G11.2−0.3, with an expansion age of 1400 – 2400 years (Borkowski et al. 2016), which has all the expected components of a young CCSN: distinct, fairly symmetric shell, and bright PWN with a jet/torus structure as often seen (Ng & Romani 2004) containing a 65 ms pulsar.

In principle, the youngest objects should provide the most information about their birth events, their immediate surroundings, and the nature of the freshly created pulsars. Much of that information is accessible through study of X-ray emission of a few keV energy: thermal X-ray emission from ejecta and swept-up ambient medium, and the spectrum and morphology of the non-thermal emission from the PWN. The pulsar itself may be detectable in X-rays. An analysis of early \textit{Chandra} observations of G11.2-0.3 (Roberts et al. 2003) found possible evidence for a hard, perhaps non-thermal, spectral component in the shell, while characterizing the PWN spectrum between 1 and 10 keV. But \textit{Chandra}’s bandpass, while ideal for thermal emission, is not wide enough to allow firm conclusions to be drawn on the spectral slope (and spatial structure) in the PWN, or to clearly separate any non-thermal emission from the shell’s thermal emission. These analyses become much more straightforward at higher energies, in the range ideally suited to \textit{NuSTAR}.

An in-depth analysis of a 400 ks \textit{Chandra} observation of G11.2-0.3 found a number of puzzles (Borkowski et al. 2016). The shell spectrum indicates a large swept-up mass. Expansion into a uniform medium, or into a steady spherical wind ($\rho \propto r^{-2}$), are ruled out by evolutionary considerations. But a combination of morphological and spectral information on the shell interior implies that the reverse shock has already returned to the center of the remnant, confining and compressing the PWN. The PWN itself shows no significant spectral steepening as one moves away from the pulsar, unlike most other PWNe (e.g., Bocchino & Bykov 2001). This fact has implications for the nature of particle transport in PWNe.

While many of these questions require examination of the thermal emission, non-thermal emission at higher en-
ergies can address issues of particle acceleration in both the shell and PWN and of PWN evolution. If the shell of G11.2-0.3 has no associated synchrotron X-ray emission, G11.2-0.3 will be alone among remnants less than a few thousand years old in this property. Borkowski et al. (2016) found blast-wave velocities from direct expansion of 700 – 1200 km s$^{-1}$, fast enough to allow electron acceleration to X-ray-emitting energies. The confirmation and spectral characterization of such emission is important for the study of shock acceleration. The PWN is also one of the youngest known, and its spectral properties above the Chandra band are important for the study of particle acceleration in relativistic shocks and transport into the PWN interior.

Power to the PWN is provided by the central rotation powered pulsar (PSR). How exactly the pulsar manages to produce its wind and how this wind becomes particle dominated are questions that are still unanswered, but observational properties of the engine can shed light on the problem by providing clues to the geometry of particle acceleration in the magnetospheres. J1811-1925 is a radio-quiet, $\sim 65$ ms, high-magnetic field pulsar with a field strength of $B \sim 10^{12}$ G and an estimated rotational kinetic energy loss of $\dot{E} \sim 6 \times 10^{36}$ ergs s$^{-1}$ (Torii et al. 1999). It was discovered in soft X-rays by ASCA (Torii et al. 1997) and in the soft (20 – 300 keV) $\gamma$-ray band by INTEGRAL/IBIS (Dean et al. 2008). Many PWN have proven themselves to be effective accelerators, and due to proximity, it was postulated whether J1811-1925 could be related to the nearby TeV source HESS J1809-193, but the association was deemed unlikely due to the distance from the TeV emitter and the fact that the jet of J1811-1925 is not pointed towards HESS J1809-193, in which case it becomes hard to explain how the particles are propagating to the target. It remains undetected in radio (Crawford et al. 1998) and in the GeV by the Fermi LAT (Acero et al. 2016), which makes the X-ray band the only accessible for study.

The hard x-ray properties of the pulsar have been previously studied with RXTE (Roberts et al. 2004), where it was seen that the pulse profile maintained its sinusoidal shape up to 90 keV, and the pulsed spectrum was measured in the PCA (2.5 – 30 keV) to be a power-law with slope $\Gamma = 1.16 \pm 0.2$. Later, the data from RXTE was combined with INTEGRAL (Kuiper & Hermsen 2015), confirming pulsations up to 135 keV, and the spectrum of the remnant + pulsar above 20 keV to be consistent with a power-law of $\Gamma = 1.61 \pm 0.15$.

In this paper we undertook a detailed study of G11.2-0.3 with NuSTAR to examine the pulsar, PWN, and shell. For the pulsar, we examined the pulse profiles as a function of energy and the spectrum of pulsations. For the PWN, we examined the integrated spectrum and energy-dependent morphology. Finally, for the shell, we attempted to confirm the presence of non-thermal emission in the shell and to study it if confirmed.

2. OBSERVATIONS AND DATA REDUCTION

We use in this paper data from NuSTAR (Harrison et al. 2013), Chandra (Weisskopf et al. 2002), and INTEGRAL (Ubertini et al. 2003). The NuSTAR data was taken from June 23 to June 26, 2016 for a total on target exposure time of 89ks after filtering.
3. ANALYSIS

We will first present the analysis of the pulse profile, §3.1 then the analysis of the geometrical properties of the remnant §3.2 both of which were performed with NuSTAR data only. The spectral analysis section will address separately in order; the full remnant broad band spectrum, §3.3.1 the nebula spectrum, §3.3.2 the pulsed spectrum, §3.3.3 and finally the broadband spectral energy distribution (SED) from 1 – 300 keV, §3.4.

3.1. Pulse profile

We applied barycenter corrections to the event file using the the NuSTAR clock-correction file version 32 (or newer) at the position of the pulsar as given by Chandra. The extracted source counts from a 123′′ radius circular region (corresponding to 50 pixels) and added FPMA and FPMB counts together. We applied the ephemeris provided by Smith et al. (2008) which was obtained from RXTE, and folded the lightcurve, but did not recover the pulsations. We then used HENDRICS (Bachetti 2015), built on Stingray (Huppenkothen et al. 2016), to find a new local solution and PINT to calculate the errors (Luo et al. 2015). We obtain a frequency of ν = 15.4564269(1) Hz and $\dot{\nu} = -8.2(2)\times10^{-12}$ Hz s$^{-1}$ at the epoch T$_0=57563$ MJD. We then chose 5 different energy bins, selected to have an equal amount of counts in each bin after background subtraction to get the pulse profiles shown in Figure 1. The energy bins each contain ~ 7800 counts and are: 3.00 – 4.36, 4.36 – 6.00, 6.00 – 8.08, 8.08 – 11.68, and 11.68 – 35.00 keV. The integrated flux at pulse peak remains approximately constant throughout the five bins, while the off-pulse flux decreases, causing the pulse to broaden. We calculate the pulse fraction as $PF = (F_{\text{max}} - F_{\text{min}})/(F_{\text{max}} + F_{\text{min}})$, where $F_{\text{min}}$ is the minimum flux in the pulse profile and $F_{\text{max}}$ the maximum flux in the profile. The resulting curve, shown in Figure 2, can be fit with an exponential that flattens above 25 keV. Since the pulse fraction is a measure of the ratio of the pulse to the steady PWN component, the curve shows the PWN flux growing fainter with respect to the pulsed component as a function of increasing energy.

3.2. Imaging

To investigate the energy-dependent remnant geometry, we first divided each FPM into three energy bands chosen to have equal amounts of counts after background subtraction. The background was obtained adjacent to the source, as well as a transient source located at RA=272:49:16.93 and Dec=−19:28:23.16, which appeared briefly between 2016 June 24 at 22:57:00 UTC and 2016 June 25 at 00:20:00 UTC, but the source itself is clear of contamination, and a clean background region could be obtained adjacent to the source. The details of each extracted spectrum will be visited in the relevant sections. NuSTAR flies two co-aligned telescopes with two identical detector focal planes that we will refer to as FPMA and FPMB.

Chandra data used here were obtained in five segments between May 5 and September 9, 2013 for a total effective exposure of 388 ks after screening, as described in Borkowski et al. (2016). Data were obtained in Very Faint mode, and reprocessed with CIAO v4.6 and CALDB v4.6.3. Screening for periods of high particle background was performed. The five observations were aligned as described in Borkowski et al. (2016). For spectral analysis, the background had to be obtained from the Chandra blank fields, available through the Chandra CALDB. This was necessary, because the source contaminates the entire S3 CCD chip, most likely due to dust scattering, which will be significant at column densities above $1\times10^{22}$ atoms cm$^{-2}$.

We obtained the INTEGRAL ISGRI/IBIS data and responses on PSR J1811+1925 (we note that in the catalog it is labeled as PSR J1811+1926) from the INTEGRAL General Reference Catalogue v.41 Ebisawa et al. (2003).
was obtained as optimal by measuring the PSFs of deconvolved point sources and finding that no further improvement was obtained in PSF width beyond this value (for details see Madsen et al. 2015). After the deconvolution we combined FPMA and FPMB images. Figure 3 shows the three energy bands for the two selections. Since each image contains the same amount of photons, and the stretch of each image is the same from peak to background, the apparent dimming of the remnant with respect to the central PWN is real. There is also an indication in the off-pulse images that the PWN is shrinking with increasing energy. To investigate this in more detail, we extracted a $350''$ strip along RA with a width of $17''$ in Declination through the pulsar (see Figure 4) and summed across the short axis. Figure 5 shows the intensity profile strips normalized to the total number of counts present in the strip in a linear plot to emphasize how the intensity across the remnant becomes more centralized with increasing energy. It also shows that the peak of the intensity is shifting east. In Chandra, Borkowski et al. 2016 finds the maximum intensity of the jet below 8 keV to be located West of the pulsar location, which is in agreement with our findings.

Above 8 keV we see the intensity on the east side of the pulsar decreasing and the maximum intensity localized around the pulsar. We note that since the pulse profile broadens at higher energies, it is possible that there is some pulsar contamination present at the edges of the off-pulse window that could bias the peak intensity towards the pulsar location.

To determine the shrinkage rate in the remnant as a function of energy, we defined two axis; one along the ‘jet axis’ (estimated from Chandra images to be $340^\circ$), and one that is perpendicular, which we call the ‘torus axis’. We rotated the images by $340^\circ$ and again extracted an intensity strip $350''$ long and $17''$ wide (see Figure 4) from each energy band and plot them together in Figure 6, where we have this time normalized each profile at the pulsar location, which we identify as the geometrical center of the remnant. It should be noted that the maximum intensity is not found at the pulsar location, but off-center along the jet axis as already discussed. We measure the Half Width at Half Max (HWHM) from the pulsar in arcseconds.

Because the deconvolution procedure does not offer an absolute error on how well it has managed to recreate the correct lengthscale, we deconvolved several strong point sources in the same energy band and noted that their PSF after deconvolution changed by about $1.5''$ between the lowest and highest band. This gives us a conservative $2''$ relative error between energy bands. We weighted the HWHM bins with the number of counts for an asymmetric center of the bin, and fitted the HWHM as a function of energy with a power-law: $kE^{-\gamma}$ (see Figure 7). The averaged East and West exponent for the jet is $\gamma_{\text{jet}} = 0.9 \pm 0.3$, and for the torus axis $\gamma_{\text{torus}} = 0.5 \pm 0.4$. Unfortunately, the uncertainties on the function are quite large, but we can still deduce that the central parts of the remnant appear to shrink faster along the jet axis (East-side side more rapidly than the West) than the torus axis (South-side more rapidly than the North).

3.3. Spectroscopy
Fig. 5.— Strip extracted along RA 350′′ long and 17′′ across (see Figure 4) through the pulsar position and summed across the short axis. The strips have been normalized to the total number of counts in the strip and shows that the intensity becomes more concentrated at the center of the remnant with increasing energy.

With Chandra, Roberts et al. (2003) characterized and measured the spectrum across the remnant using a plane-parallel shock model (Borkowski et al. 2001) and a power-law to account for a hard excess. They observed significant variations across the remnant, however, the results suffered from a partial degeneracy between the absorbing column, the electron plasma temperature, and the power-law index. NuSTAR has little sensitivity to the absorbing column and the abundances in the remnant, but with its wider bandpass it can constrain the power-law index.

To overcome these shortcomings in both instruments, we supplement the NuSTAR data with Chandra where it benefits.

We use XSPEC for fitting (Arnaud 1996), Wilms abundances (Wilms et al. 2000), Verner cross-sections (Verner et al. 1996), and C-stat as the fitting statistic (Cash 1979) on the un-binned data, but report the goodness of fit for the NuSTAR spectra only, since, as shall be explained, it was not feasible to do so for the combined Chandra-NuSTAR fit. Unless otherwise stated the errors will be reported at the 90% confidence limit.

3.3.1. Full remnant broadband spectrum

While G11.2-0.3 is a complex object with at least three distinct components (PSR, PWN, and shell) we first describe a fit to the spatially integrated emission for comparison with non-imaging instruments such as NICER and INTEGRAL. We extracted the broadband spectrum from both observatories for the entire remnant within 123″, including both the PSR and PWN. The PSR is marginally piled up in Chandra, but the skew to the spectrum is minor enough that qualitative assumptions about the spectral shape can still be made if we ignore energies above 5 keV for Chandra. In NuSTAR we have signal up to 35 keV, but since the background becomes comparable to the source at ~25 keV we fit conservatively from 3 – 20 keV.

We model the spectra with an absorbed\(^5\) power-law and a plane-parallel shock model, given in XSPEC notation as: `tbabs(powerlaw+vpshock)`. We found the upper limit of the ionization timescale, \(\tau_u\), to be degenerative with the electron plasma temperature and froze it to \(\tau_u = 4.2 \times 10^{11}\) s cm\(^{-3}\) as found by Roberts et al. (2003). Choosing a \(\tau_u\) that is 50% lower increases the electron temperature by \(\sim 10\%\). Separately, each instrument fits this model well, but as already discussed, the NuSTAR data offers poor constraints on the shock component, while the Chandra data poorly constrains the power-law component. The best fit values therefore, unsurprisingly, differed significantly between instruments. However, when fitted together, we discovered that this discrepancy isn’t just due to the different energy bands, but because there are significant residuals in the transition region between the thermal and non-thermal component between 5 – 7 keV as shown in Figure S5 middle panel, which appears like a ‘break’ in the continuum.

As reported by Madsen et al. (2017), cross-calibration differences are known to exist between the two observatories, mainly in the absolute normalization, but also in the slopes of the two instruments. However, it is important to note that the feature is seen only in NuSTAR well outside the Chandra band and not directly in the overlap region, which is where typically cross-calibration issues show themselves. Unfortunately, dedicated campaigns between NuSTAR and Chandra only exist for the gratings and we can therefore not rule out that this feature could stem from a cross-calibration issue. There are strong indications, though, that this is not the case. A ~9 keV break was detected in G21.5-0.9 with NuSTAR (Nynka et al. 2014), and breaks across the Crab PWN were seen between 8 – 12 keV also exclusively with NuSTAR data (Madsen et al. 2015). In MSH 15-52 a break was detected around 6.3 keV (An et al. 2014), and like for G11.2-0.3, this one was only found when combined with Chandra data. Outside of PWN spectra, we have not observed breaks like this between NuSTAR and Chandra data, and we therefore proceeded under the assumption that this is not a cross-calibration issue, but an actual problem with the chosen models.

A better fit was obtained by replacing the power-law with a broken power-law and setting the break energy around ~6 keV (see Figure S8 bottom panel). This improved model still exhibits residuals around 5 – 6 keV, where we introduced the break, but they may be explained by a far more gradual transition than the sharp cusp of the broken power-law. As to the source of the break, one possibility is that the thermal component is poorly represented by a single shock and rather should be a superposition of several different electron temperatures and abundances. This is supported by the very large residuals seen in our abundance lines of Mg, Si, S, Ar and Ca. Lopez et al. (2011) measured abundances at 23 locations across the remnant and found the abundances and electron temperatures can vary by factors of 2. Adding more vpshock components indicated that these residuals could be improved, but it introduced a large number of free parameters and degeneracy that raised its own complications. We therefore continued with the broken

\(^5\)http://psr.sternwarte.uni-erlangen.de/wilms/research/tbabs/
power-law interpretation, noting that the power-law index, $\Gamma_1$, below the break energy has little physical meaning.

In the initial modeling we allowed the abundances to remain free and find relative to solar: Mg~1.2, Si~1.5, S~1.3, Ar~1.2, and Ca~2.9. These abundances are acceptably close to average abundance values inferred from Lopez et al. (2011), but as stated the fit leaves significant residuals in the lines. These residuals can be cosmetically improved upon by adding a number of gaussians, but since we already understand the reason for the residuals, and the application of multiple gaussians is unphysical, we left the residuals as they are.

At this point we therefore emphasize that the inclusion of the Chandra data serves to better define the power-law by providing constraints on the thermal component and the galactic absorption. It is not our intent to make any detailed measurements or statements on the abundances values, which has already been covered in detail by Roberts et al. (2003), Lopez et al. (2011), and Borkowski et al. (2016). Instead, we focus here on the hard non-thermal component, represented by $\Gamma_2$, which is the index above the power-law break.

We proceeded to freeze the abundances and calculated errors for all relevant parameters, noting that it became necessary to evaluate the electron temperature from the $\chi^2$-curve produced by the steppar command due to the complications from the line residuals. For the entire remnant, including the PSR, we find the best fit parameters: $N_H=3.35\pm0.01$, $kT = 0.65\pm0.01$, $E_{\text{break}} = 5.9\pm0.3$, $\Gamma_1 = 1.2\pm0.1$, and $\Gamma_2 = 1.78\pm0.03$ (see Table 1).

3.3.2. Nebula and Shell Spectrum

To investigate the PWN spectrum, we separated out the PSR from the nebula in the NuSTAR data by employing phase-resolved spectroscopy. This is necessary due to fact that the NuSTAR PSF, which has a Half
Power Diameter (HPD) of 60″, will otherwise contaminate the remnant with the PSR. We used the ephemeris presented in section 3.1 to extract the counts from phase bins 0.6 – 1.0 (see Figure 1), which we define as the off-pulse phase. As shown in Figure 9, we extracted three regions for both instruments: 0 – 37″ (#1), 37 – 74″ (#2), and 74 – 123″ (#3), which cover the central PWN, the shell, and what is between. Because the shell, # 3, has very little contamination from the pulsar, confirmed by the absence of pulsations when folding the spectrum on the period and verifying identical fits within errors to the pulse-on and pulse-off spectrum, we used the full phase range (0.0 – 1.0) to increase statistics. For NuSTAR the response files are obtained out of the standard pipeline for extended regions. Since PSF corrections cannot be applied to extended responses in NuSTAR, the flux will not be precise between instruments, and we allowed for a constant to account for the flux differences between FPMA and FPMB and another for Chandra.

Based on our findings above, we used the broken power-law model, `bknpowerlaw + vpshock`, and found that in all three cases it is required. The line residuals in Chandra still dominate the fit statistics and we followed the procedure outlined before and froze the abundances once the residuals had been minimized. We summarize the fit results in Table 1 and find that $\Gamma_2$ softens with increasing radius, progressing from region the PWN ( #1) through to the shell ( #3) from 1.06 ± 0.05 to 2.1 ± 0.1, which supports the scenario of the remnant becoming fainter with increasing radius and energy.

As a separate check, we fitted the NuSTAR data alone, which required us to freeze the $N_H$ and abundances to the value found with Chandra for each region and the upper ionization timescale to $\tau_u = 4.2 \times 10^{13}$ s cm$^{-3}$, neither of which are sensitive, or can be constrained, in the NuSTAR band. The fits to the NuSTAR data alone are given in Table 2 and show that within errors the photon index is consistent with that found for $\Gamma_2$ in Table 1.

For the PWN (region #1) we cannot measure a thermal component in NuSTAR.

To quantify the broken power-law spectrum better, we also fitted the combined spectra with a power-law in place of the broken power-law and did one fit with the power-law photon index left free, and another fixing the photon index to $\Gamma_2$ from the broken power-law found in the same region. The ratio plots for all three regions are shown in Figure 10 and 12. In the upper panels we show the broken power-law fit, in the middle panel the power-law fit, the results of which we do not record since they are for visual purposes only, and in the bottom panel the power-law fit with $\Gamma = \Gamma_2$ frozen. By considering the ratios in each region, it appears that the broken power-law spectrum is strongest in the shell.

Finally, we fitted the spectra in the shell with a `vpshock+srcut` model, where `srcut` describes the synchrotron spectrum from an exponentially cut-off power-law distribution of electrons in a homogeneous magnetic field. We used the values for the radio spectral index, $\alpha = 0.56$, and normalization of the radio flux at 1 GHz of 2 Jy, obtained from Tam et al. (2002), but the curvature of the spectrum at high energies is far too quick to describe the data.

We searched for an iron line in the NuSTAR data, but find no evidence of its presence. Despite background and pileup issues around the iron region, we also searched the Chandra data since a line should still be evident even if the continuum is piled-up, but do not find any evidence of iron there either.
3.3.3. Pulsed spectrum

From the imaging analysis it is apparent that the PWN contributes less flux at higher energies, which is supported by the pulse fraction curve, showing the ratio of the PSR flux to PWN flux increasing as a function of energy. To investigate the shape of the pulsed spectrum, we used as background the off-pulse phase (0.6 – 1.0) and subtracted it from the on-pulse phase (0.0 – 0.6). To test the stability of the results, we used three different extraction regions: the entire remnant (123″), an intermediate region (74″), and the interior (37″). They agree within errors, so we used the highest SNR spectrum from a radius of 74″. Because the background is contained in the same region, which reduces the uncertainties, we were able to measure the spectrum all the way up to 50 keV. We fitted the spectrum with two models: a powerlaw and logpar model, which is a power-law model where

\[
F(E) = K(E/E_1)^{(\alpha + \beta \log(E/E_1))} \text{ph cm}^{-2} \text{s}^{-1} \text{keV}^{-1}.
\]

Here \(\alpha\) is the photon index at the pivot energy \(E_1\), and we set \(E_1 = 5\) keV. The results of the two models are shown in Table 1, and while the logpar model yields a slightly better fit, the difference between the two models is only significant to 98%.
3.4. Broadband SED

Armed with this understanding of the PWN and PSR, we then proceeded to fit the spectrum of the entire remnant, PWN+PSR, (here we include the shell together with the PWN) across Chandra, NuSTAR, and INTEGRAL, from 1 – 300 keV. To help with the stability of the spectrum and to illustrate how the different components interact, we included four spectra from NuSTAR: the full phase (phase: 0 – 1.0), on-pulse period (phase: 0.0 – 0.6), off-pulse period (phase: 0.6 – 1.0), and the pulse on-off spectrum.

We fit the model $v_{\text{pshock}} + \text{bknpowerlaw}(\text{PWN}) + \text{powerlaw}(\text{PSR})$ and set the normalization of the PSR to 0 in the off-pulse spectrum, and the normalization of the PWN (thermal and non-thermal) to 0 for pulse on-off spectrum. As before we freeze the $\Gamma_{\text{PSR}}$, $\Gamma_{\text{PWN}}$, $I_{\text{PSR}}$, and $I_{\text{PWN}}$ to 0 for pulse on-off spectrum. As before we freeze the normalization of the PWN (thermal and non-thermal) to 0 in the off-pulse spectrum, and the normalization of the PSR to 0 in the pulse on-off spectrum. We can collect our findings in three categories: the PSR, PWN, and the shell.

We find that the pulsed spectrum can be described by a power-law with photon index $\Gamma = 1.35 \pm 0.08$ all the way through the INTEGRAL/IBIS band up to 300 keV. At 20 keV the contribution of PWN+shell and PSR to the total flux is roughly 50/50, but at higher energies, the pulsed spectrum dominates the combined flux of the remnant and becomes the primary contributor in the soft γ-rays. The pulsed spectrum is consistent with the measurement made with RXTE reported by Roberts et al. (2004), and the interpretation of the pulsed flux dominating above 20 keV consistent with previous RXTE and INTEGRAL findings by Kuiper & Hermsen (2015).

It is commonly accepted that the sources of the high-energy radiation in rotation powered pulsars are curvature and synchrotron photons from pair production cascades in the magnetosphere. However, the site of the acceleration has long been a matter of debate, and though it still remains uncertain, Fermi re-solved the long-standing question of whether the acceleration originated close to the stellar surface from the polar cap region (Daugherty & Harding 1982) or in the outer magnetosphere at the light cylinder (where the velocity of the co-rotating magnetic field equals the speed of light), as in the outer-gap region (Cheng et al. 1986) and the slot-gap
region along the current layers at the boundary between closed and open field lines (Arons 1983). Magnetic pair production in the strong fields along the polar cap predicts steep, super-exponential absorption cut-offs in the γ-ray spectra above a few GeV, which have not been observed. Instead, Fermi detected pulsars typically exhibit hard photon spectra at a gradual decline at several tens of GeV (Abdo et al. 2010; Abdo et al. 2013). Despite being young and bright in the X-rays, J1811-1925 has not been detected in the Fermi band. The flux of the power-law extrapolated into the Fermi/LAT band (100 MeV – 100 GeV) is \(1 \times 10^{-5}\) photons cm\(^{-2}\) s\(^{-1}\), which is well above the detection threshold limit of \(1 \times 10^{-9}\) photons cm\(^{-2}\) s\(^{-1}\) for a photon index of 1.5 given by Figure 20 in Abdo et al. (2010). This would indicate that the spectrum has a turnover below 100 MeV and makes it similar to PSR J1846–0258 (Kuiper & Herrnse 2009) also detected with INTEGRAL/ISGRI/IBIS but not by Fermi/LAT, and PSR B1509–58, which is detected above 1 MeV with a measured cutoff of a few MeV (Cusumano et al. 2001; Abdo et al. 2010; Pilia et al. 2010). Common for these three is that they all have broad, single pulsed profiles in contrast to the typical narrow double-peaked γ-ray pulsars. Recent progress in Particle-in-cell (PIC) simulations of pulsar magnetospheres indicate that the likely location of high-energy particle acceleration occurs along the current sheet at the equator in a zone close to the light-cylinder (Chen & Beloborodov 2014; Philippov et al. 2015; Philippov & Spitkovskiy 2018). In the context of these simulations, the characteristics of J1811-1925 can be understood if it has an inclined magnetic axis in the range 30–60° and is viewed at an angle of \(\sim 45°\). In this case, one observes a single peak originating from the electron populations with a spectral energy distribution that falls off faster for double peaked pulse profiles (see Figure 10, Cerutti et al. 2016). Detailed analysis performed with radio and X-rays, which take into account the shape of the torus and asymmetric brightness of the jets, indicates that the tilt of the torus to the plane of the sky is \(\sim 60°\) (Borkowski et al. 2016). The line of sight to the rotation axis is then 30° and consistent with what can be inferred from the pulse profile and cut-off of the spectrum.

The spatially integrated spectrum of the pulsar-wind nebula at energies above the Chandra band is well described by a power-law with \(\Gamma = 1.71 \pm 0.07\), consistent with the value of 1.78 \(\pm 0.7\) reported by Borkowski et al. (2016). That study found no significant steepening in spectrum with distance from the pulsar as is seen in other PWNe such as G21.5–0.9 (Nynka et al. 2014), while the nominal best-fit values of \(\Gamma\) did increase, the magnitude of the change was within errors. However, here we find that the PWN extent along the jet direction shrinks with increasing energy, with HWHM \(\propto E^{-\gamma}\) with \(\gamma_{\text{jet}} = 0.9 \pm 0.3\) along the jet axis and \(\gamma_{\text{torus}} = 0.5 \pm 0.4\) perpendicular to that direction. While errors are large, the shrinkage along the jet seems secure and larger than that perpendicular to the jet. These two results are consistent if particle transport along the PWN is primarily advective and monotonically increasing going out, in which case one expects a constant spectrum until an abrupt spectral cutoff at a distance from the pulsar corresponding to the particle lifetimes (see figures in Reynolds et al. 2003). Most PWNe show, instead, gradual steepening of the spectrum, indicating a mixture of particles of different ages at a given distance from the pulsar, such as might be produced by diffusion (e.g., Reynolds & Jones 1991; Tang & Chevalier 2012) or more complex advective motions (Porth et al. 2013). The magnitude of the energy-dependent shrinkage exponent, \(\gamma\), of about 0.9 is distinct from those measured by NuSTAR in G21.5–0.9 (Nynka et al. 2014) and MSH 15–52 (An et al. 2014), where values of \(\gamma\) of about 0.2 were found. For the Crab, Madsen et al. (2015) reported differing shrinkage rates along the jet, counterjet, and transverse (torus) directions of about 0.05, 0.2, and 0.08, respectively. Thus the jet in G11.2-0.3 stands out among PWNe in two ways: a more rapid shrinkage with energy, but absence of progressive spectral steepening along its length. Evidently the nature of particle transport in G11.2-0.3 is different from that in other very young PWNe. A deeper analysis of the PWN in Kes 75, the youngest known in the Galaxy, may cast light on this situation.

For the shell we confirm the suggestions from Chandra data that a non-thermal component is required, and can be described by a power-law with \(\Gamma = 2.1 \pm 0.1\). An srcut fit does not do well in describing the data. We also see some shrinkage of the shell radius with increasing energy, consistent with the Chandra finding that harder emission is concentrated near the inner edge of the shell (Borkowski et al. 2016). The confirmation of non-thermal X-rays from the shell means that G11.2-0.3 joins the other Galactic remnants less than a few thousand years old in having evidence for shock acceleration of electrons to multi-TeV energies. Only three Galactic shell remnants of core-collapse supernovae with ages less than about 2000 yr are known: Cas A (about 350 years old), Kes 75 (about 480 ± 50 years old; Reynolds et al. 2018b), and G11.2-0.3. The non-thermal X-ray spectrum of Cas A is remarkable, extending as a single power-law to energies of order 100 keV, with the hardest emission originating from neither the forward nor the reverse shock (Grefenstette et al. 2015). While the Chandra spectrum of the shell in Kes 75 requires a hard spectral component, that component may be a power-law (Helfand et al. 2003) or a high-

### TABLE 3

| parameter | tbabs | powerlaw (PSR) | powerlaw (PWN) | vphabs |
|-----------|-------|----------------|----------------|--------|
| \(N_T\) | \(1.34 \pm 0.08\) | \(3.9 \pm 0.8 \times 10^{-4}\) | \(2.01 \pm 0.08\) | \(3.6 \pm 0.8 \times 10^{-4}\) |
| \(\tau_{\gamma}\) | \(4.2 \times 10^{11} \text{cm}^{-2}\) | \(1.34 \pm 0.08\) | \(3.9 \pm 0.8 \times 10^{-4}\) | \(2.01 \pm 0.08\) |

\(a\) \(\tau_{\gamma} = 4.2 \times 10^{11} \text{cm}^{-2}\), abundances relative to solar: \(\text{Mg} = 1.1\), \(\text{Si} = 1.4\), \(\text{S} = 1.2\), \(\text{Ar} = 1.1\), \(\text{Ca} = 2.7\).

\(b\) \(10^{22}\) atoms \text{cm}^{-2}\)

\(c\) photons \text{keV}^{-1} \text{cm}^{-2}\)

\(d\) With Chandra data removed
For an age of 2000 years and a break frequency of 3 Hz, we find $\nu_{t,2000}$ years allows the deduction of that higher magnetic-strength, our knowledge of the age of G11.2−0.3 of about 0.5. Of all the known cases of shell synchrotron X-rays, only G11.2-0.3 shows such a small amount of steepening. The value $\Delta \alpha = 0.5$ is of course the expectation for the very simple case of continuous electron acceleration to very high energies followed by radiative losses in a homogeneous source. Synchrotron losses simultaneous with acceleration will produce an electron spectrum with an (approximately) exponential cutoff at an energy at which the acceleration time equals the loss time (Zirakashvili & Aharonian 2007), rather than a steeper power-law. The sum of a range of cut-off spectra can produce a power-law.

An attempt to model the integrated spectral-energy distribution (SED) of the shell emission of G11.2-0.3 with a simple loss model encounters severe quantitative difficulties. If we take our observed value of $\Gamma$ at face value, the extrapolations of the radio spectrum ($S_{\nu} \sim 20(\nu/1 \text{ GHz})^{-0.5}$) up and the X-ray spectrum down meet at a frequency of about $3 \times 10^{12}$ Hz. If we picture electrons as accelerated in a region in which the magnetic field allows energies of $\sim 100 \text{ TeV}$ to be reached, but then radiating subsequently in a region with higher field strength, our knowledge of the age of G11.2-0.3 of about 2000 years allows the deduction of that higher magnetic-field strength. The half-life $t_{1/2}$ of an electron radiating the peak of its synchrotron spectrum at frequency $\nu$ in a magnetic field $B$ is given by

$$t_{1/2} = 5.69 \times 10^{11} B^{-3/2} \nu^{-1/2} \text{ s.}$$

(4)

For an age of 2000 years and a break frequency of $3 \times 10^{12}$ Hz, we find

$$B = 300 \left( \frac{t}{2000 \text{ yr}} \right)^{-2/3} \left( \frac{\nu}{3 \times 10^{12} \text{ Hz}} \right)^{-1/3} \mu\text{G.}$$

(5)

This value is quite high, perhaps implausibly so.

This naive picture is almost certainly incorrect. The maximum photon energy emitted by an electron distribution limited by radiative losses depends only on the shock velocity and magnetic field, which (geometric factors likely to be of order unity; e.g., Reynolds et al. 2008): $h\nu_{\text{max, loss}} \sim 0.2 u_{s}^{2}$ keV where $u_{s}$ is the shock speed in units of $10^{8} \text{ cm s}^{-1}$. For G11.2-0.3, proper-motion observations give $u_{s} \sim (0.7 \pm 1.2)$ (Borkowski et al. 2010), so it is impossible to produce the observed $20 \text{ keV}$ synchrotron photons from an electron distribution accelerated in a region with a magnetic-field strength of 300 $\mu$G.

But the interpretation of the integrated SED of G11.2-0.3 as that of a power-law steepened by continuous losses already requires that the conditions in the acceleration region be different from those in the regions where the electrons do most of their radiating. To produce synchrotron photons up to the $\sim 20 \text{ keV}$ we observe from the radiating region where $B \sim 300 \mu$G, we require electron energies up to $E_{m} \sim 60 \text{ TeV}$. The loss-limited maximum electron energy is roughly $E_{\text{max}} \sim 100u_{s}B^{-1/2}$ TeV; since $u_{s} \sim 1$, we require a very low magnetic field in the acceleration region, of order $1 \mu$G. The combination of a very low field near the shock, where electrons are presumably accelerated, followed by their diffusing or advecting into a region where $B$ is larger by orders of magnitude, seems extremely implausible. Much more likely is that the X-ray photon index reflects not the spectrum radiated by a single power-law electron distribution, but the superposition of distributions accelerated under a range of conditions, with the rough agreement of $\alpha_{e} + 0.5$ with the X-ray energy index $\Gamma - 1$ entirely fortuitous.

5. CONCLUSIONS

Our NuSTAR observations extend the range of X-ray studies of G11.2-0.3 to 35 keV, with new results on the pulsar, the pulsar-wind nebula, and the outer shell. The PSR shows a pulse profile broadening with increasing energy, and an increasing pulsed fraction, and its spectrum does not show evidence of curvature up to 300 keV. The PWN has an integrated spectrum consistent with earlier studies, but shows shrinkage along the jet direction, which contrasts with the lack of observed spectral steepening along the jet in Chandra observations. The electron outflow in the PWN may be simpler than that seen in other young PWNe. Our imaging observations of the shell show a slightly smaller radius at higher energies, consistent with Chandra results. We confirm the existence of a hard, power-law component from the shell of G11.2-0.3, with photon index $\Gamma = 2.1 \pm 0.1$, which is almost certainly synchrotron emission, given the absence of significant Fe K$\alpha$ emission between 6.4 and 6.7 keV. While this value of $\Gamma$ agrees with the expected value for the index of synchrotron emission from a simple model of synchrotron losses in a homogeneous source given the radio (energy) spectral index of 0.6, the implied “break” frequency of $3 \times 10^{12}$ Hz demands an impossibly high magnetic field, and the agreement is likely fortuitous. Instead, we attribute the hard spectrum to a superposition of spectra from electrons accelerated in different regions with different conditions, which may also explain the broken spectrum of the power-law.

Facilities: NuSTAR Chandra INTEGRAL

This work was supported under NASA Contract No. NNG08FD60C, and made use of data from the NuSTAR mission, a project led by the California Institute of Technology, managed by the Jet Propulsion Laboratory, and funded by the National Aeronautics and Space Administration. We thank the NuSTAR Operations, Software and Calibration teams for support with the execution and analysis of these observations. This research has made use of the NuSTAR Data Analysis Software (NuSTARDAS) jointly developed by the ASI Science Data Center (ASDC, Italy) and the California Institute of Technology (USA). We would also like to thank Robert Archibald for his help with finding the timing solution.
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