Photoproduction in Ultra-Peripheral Heavy Ion Collisions at STAR

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We present recent STAR results on photoproduction in ultra-peripheral relativistic heavy ion collisions. In these collisions the impact parameter of the beam particles is larger than the sum of their nuclear radii, so that they interact via their long-range Coulomb fields. STAR has measured the production of $\rho^0(770)$ mesons in exclusive reactions as well as in processes with mutual nuclear excitation of the beam particles. We present results for the $\rho^0$ production cross section in Au-Au collisions at $\sqrt{s_{NN}} = 200$ GeV for coherent as well as incoherent coupling. The dependence of the cross section on the $\rho^0$ rapidity is compared to theoretical models. We also studied the ratio of coherent $\rho^0$ to direct $\pi^+\pi^-$ production as well as the $\rho^0$ helicity matrix elements and we observe interference effects in the $\rho^0$ production. In addition STAR has measured the production of $\rho^0$ mesons in d-Au collisions at $\sqrt{s_{NN}} = 200$ GeV and that of $e^+e^-$-pairs in Au-Au at $\sqrt{s_{NN}} = 200$ GeV. We also see an enhancement around 1510 MeV/$c^2$ in $\pi^+\pi^-\pi^+\pi^-$ final states in Au-Au collisions at $\sqrt{s_{NN}} = 200$ GeV.

1. Introduction

Heavy ions are surrounded by a cloud of virtual photons. The electromagnetic field of a relativistic nucleus can be approximated by a flux of quasi-real virtual photons using the Weizs"acker-Williams approach \cite{1}. Since the number of photons grows with the square of the nuclear charge, fast moving heavy ions can generate large photon fluxes. Beams of heavy ions can thus be used as photon sources or targets. Due to the long range of the electromagnetic interactions, they can be separated from the hadronic interactions by requiring impact parameters $b$ larger than the sum of the nuclear radii $R_A$ of the beam particles. These so-called Ultra-Peripheral heavy ion Collisions (UPCs) allow to study photonic effects as well as photon-photon interactions \cite{2}.

A typical photonic reaction is the production of vector mesons. In this process the virtual photon, that is emitted by the “spectator” nucleus, fluctuates into a virtual $q\bar{q}$-pair, which scatters elastically off the “target” nucleus, thus producing a real vector meson. The scattering can be described in terms of soft Pomeron exchange. Figure \textsuperscript{11} illustrates this reaction taking as an example the most abundant process, the photnuclear production of $\rho^0(770)$ mesons.

The cross section for vector meson production depends on the way the virtual $q\bar{q}$-pair couples to the target nucleus. This is mainly determined by the transverse momentum $p_T$ of the produced meson. For small transverse momenta of the order of $p_T \lesssim 2h/R_A$ the $q\bar{q}$-pair couples coherently to the entire nucleus. This leads to large cross sections which depend on the nuclear form factor $F(t)$ and which scale roughly with the atomic number $A$ squared. For larger transverse momenta the $q\bar{q}$-pair couples to the individual nucleons in the target nucleus. This “incoherent” scattering has a smaller cross section that scales approximately with $A$ modulo corrections for nuclear absorption of the meson.

Due to the intense photon flux, it is possible for the vector meson production to be accompanied by Coulomb excitation of the beam particles. The excited ions mostly decay via the emission of neutrons which can be measured by the Zero Degree Calorimeters (ZDCs) of the STAR setup. To lowest order events with mutual nuclear breakup are described by three-photon
the TPC that allows to trigger on charged particles is an array of 240 scintillator slats surrounding used: the Central Trigger Barrel (CTB) \cite{6}, which 85 %. For triggering two detector systems were 100 MeV/c.

magnetic field. For tracks with pseudorapidity \eta < 1.2 and transverse momentum \pt > 100 MeV/c the tracking efficiency is better than 85 %. For triggering two detector systems were used: the Central Trigger Barrel (CTB) \cite{6}, which is an array of 240 scintillator slats surrounding the TPC that allows to trigger on charged particles in the event, and the two zero degree calorimeters, which are located at ±18 m from the interaction point and measure neutrons originating from nuclear breakup.

2. Photonuclear \rho^0 Production

STAR uses two kinds of triggers to select UPC events. The CTB-based “topology” trigger requires a low total charged particle multiplicity and divides the CTB detector into four azimuthal quadrants. Events are recorded when the left and right quadrants have coincident hits, selecting roughly back-to-back pion pairs. The top and bottom quadrants serve as a cosmic ray veto. The “minimum bias” trigger selects events where both nuclei dissociated by requiring coincident energy deposits in both ZDCs.

In the offline analysis the events were required to have two tracks of opposite charge that form a common (primary) vertex. In addition we demanded a low overall track multiplicity in order to suppress backgrounds from beam-gas interactions, peripheral hadronic interactions, and pile-up events. The primary vertex was confined to a region close to the interaction diamond which reduces contaminations from pile-up events, beam-gas interactions, and cosmic rays. The latter background component was decreased further by either excluding events around \yp = 0 in the topology data sample or by requiring neutron signals in the ZDCs as in the minimum bias trigger. The contamination from peripheral hadronic interactions was in addition suppressed by demanding the track pair to have low net transverse momentum. The backgrounds from two-photon e^+e^- (cf. section \ref{sec:2}) and photonuclear \omega production are negligible.

The \pi^+\pi^- invariant mass distributions are fit with the function

\[
\frac{\mathrm{d}\sigma}{\mathrm{d}M_{\pi\pi}} = \left| A \frac{\sqrt{M_{\pi\pi}M_{\rho}}}{M_{\pi\pi}^2 - M_{\rho}^2 + iM_{\rho}\Gamma} + B \right|^2 + f_{\text{BG}}
\]

with \Gamma(M_{\pi\pi}) \equiv \Gamma_{\rho} \frac{M_{\rho}}{M_{\pi\pi}} \left[ \frac{M_{\pi\pi}^2 - 4m_{\pi}^2}{M_{\rho}^2 - 4m_{\pi}^2} \right]^{\frac{1}{2}} \quad (2)

Equation (2) consists of a relativistic Breit-Wigner with amplitude \(A\), that describes the re-
onant $\pi^+\pi^-$ production, and a mass-independent amplitude $B$ for the non-resonant $\pi^+\pi^-$ production, as well as a Söding interference term $I$ of the two amplitudes. The second order polynomial, $f_{BG}$, describes the combinatorial background which was estimated from like sign pion pairs.

2.1. Coherent $\rho^0$ Production in Au-Au Collisions

Coherent photonuclear $\rho^0$ production is strongly enhanced at low $p_T^\rho$. It can be separated from the incoherent production by requiring $\rho^0$ transverse momenta smaller than 150 MeV/c. Figure 2 shows the $\pi^+\pi^-$ invariant mass distribution of the minimum bias data set taken during the year 2002 run in Au-Au collisions at $\sqrt{s_{NN}} = 200$ GeV [8]. The peak contains $3 075 \pm 128_{\text{stat.}} \pm 9_{\text{syst.}}$ mb $\rho^0$ candidates.

Since in Eq. (2) the amplitudes $A$ and $B$ are free fit parameters, it is possible to extract the ratio $|B/A|$ of non-resonant to resonant $\pi^+\pi^-$ production. In Au-Au collisions at $\sqrt{s_{NN}} = 200$ GeV the ratio was measured using the minimum bias data to $|B/A| = 0.89 \pm 0.08_{\text{stat.}} \pm 0.09_{\text{syst.}}$ GeV$^{-1/2}$ [8]. As expected the ratio shows no dependence on the $\rho^0$ rapidity nor on the $\rho^0$ decay angles. The value is compatible with an earlier result of $|B/A| = 0.81 \pm 0.08_{\text{stat.}} \pm 0.20_{\text{syst.}}$ GeV$^{-1/2}$ from the year 2000 run at $\sqrt{s_{NN}} = 130$ GeV [9]. Both values are also in agreement with the ZEUS measurements [10].

The luminosity of the minimum bias sample was measured based on the known total hadronic production cross section of 7.2 barn. With the value of $L_{\text{minbias}} = 461$ mb$^{-1}$ the cross section for coherent $\rho^0$ production accompanied by mutual nuclear excitation was estimated to be $14.5 \pm 0.7_{\text{stat.}} \pm 1.9_{\text{syst.}}$ mb$^{-1}$ within the experimental acceptance of $|y_\rho| < 1$ [8].

There are at least three models for $\rho^0$ production in ultra-peripheral collisions: The model of Klein and Nystrand (KN) [11] uses the Vector Dominance Model (VDM) to describe the virtual photon and a classical mechanical approach for the scattering on the target nucleus, based on results from $\gamma p \rightarrow \rho^0 p$ experiments. The Frankfurt, Strikman, and Zhalov (FSZ) model [12] employs a generalized VDM for the virtual photon and a QCD Gribov-Glauber approach for the scattering. The model of Gonçalves and Machado (GM) [13] is based on a QCD color dipole approach that takes into account nuclear effects and parton saturation phenomena. Only the KN model gives predictions for the rapidity dependence of the coherent $\rho^0$ production cross section accompanied by mutual Coulomb excitation, which are compared to the data in Fig. 3.

The total coherent $\rho^0$ production cross section was estimated using the $13 054 \pm 124_{\text{stat.}} \rho^0$ candidates in the data set taken with the topology trigger [8], which does not apply any restrictions on the ZDC amplitudes. Although this data sample could not be used for an absolute cross section measurement, because the trigger efficiency is only poorly known, it was possible to extract coherent cross section ratios for the different nuclear excitation states. These ratios were used to
Figure 3. Differential cross section $d\sigma/dy_\rho$ for coherent $\rho^0$ production accompanied by mutual Coulomb excitation as a function of $\rho^0$ rapidity extracted from the minimum bias data [8]. The solid line shows the KN model calculation [11].

The scale of the coherent mutual-excitation cross section values from the minimum bias sample. Figure 4 compares the obtained $y_\rho$-dependence of the coherent $\rho^0$ production cross section to the three models. Unfortunately the limited acceptance in $y_\rho$ does not allow to distinguish between different shapes of the distributions.

STAR has also measured the spin structure of the coherent $\rho^0$ production amplitudes in terms of spin density matrix elements [8]. The matrix elements were extracted from the minimum bias data by fitting the $\rho^0$ decay angular distribution in the $\rho^0$ rest frame to the theoretical prediction for unpolarized photoproduction [14]

$$
\frac{1}{\sigma} \frac{d^2\sigma}{d\cos\theta \ d\phi} = \frac{3}{4\pi} \left[ \frac{1}{2}(1 - r_{00}^{04}) + \frac{1}{2}(3r_{00}^{04} - 1) \cos^2\theta - \sqrt{2} \Re[r_{10}^{04}] \sin 2\theta \cos \phi - r_{11}^{04} \sin^2\theta \cos 2\phi \right] \tag{3}
$$

where $\theta$ is the polar angle between the beam direction and the direction of the $\pi^+$ and $\phi$ the azimuthal angle between the decay and the production plane. Since STAR does not measure the scattered beam particles, only an approximate production plane with respect to the beam direction could be reconstructed. $r_{00}^{0}$ represents the probability that the $\rho^0$ is produced with helicity 0, $r_{11}^{04}$ the interference between helicity non-flip and double-flip. Due to the ambiguity of photon source and target, $\Re[r_{10}^{04}]$, which is related to the interference between helicity non-flip and single-flip, could not be measured. Table 1 summarizes the results. The measured spin density elements are small, indicating $s$-channel helicity conservation. They are also compatible with ZEUS measurements on $\rho^0$ photoproduction from proton targets [10].

2.2. Interference Effects in Coherent $\rho^0$ Production in Au-Au Collisions

In ultra-peripheral collisions the impact parameter $b$ is typically much larger than the sum of the nuclear radii of the beam particles. The scattering of the virtual $q\bar{q}$-pair on the target nucleus, on the other hand, involves the short-
wave function. Since the ρ where the interference between the two possible like a two-source interferometer with separation nucleus 2, or vice versa. The system thus behaves to the target nucleus. Furthermore photon source and target are indistinguishable, so that either nucleus 1 emits a photon which produces a ρ at nucleus 2, or vice versa. The system thus behaves like a two-source interferometer with separation b, where the interference between the two possible amplitudes creates an entangled final state π+π− wave function. Since the ρ0 has negative parity, the two amplitudes have different sign, so that the cross section can be written as \[ \sigma(b) = |A(b, y_ρ) - A(b, -y_ρ) e^{i\vec{p}_T \cdot \vec{b}}|^2 \] (4)

where \( A(b, y_ρ) \) and \( A(b, -y_ρ) \) are the ρ0 production amplitudes for the two photon directions. The observed \( p_T^0 \) spectrum is obtained by integrating Eq. (4) over \( \vec{b} \), which is not measured in the experiment. For \( y_ρ = 0 \) the two amplitudes are equal so that

\[
\sigma(b) = \sigma_0(b) \left[ 1 - \cos(p_T^0 \cdot \vec{b}) \right]
\]

(5)

with \( \sigma_0(b) \) being the cross section without interference. From Eq. (5) it is clear that the cross section is suppressed for \( p_T^0 \lesssim 2h / \langle b \rangle \), where \( \langle b \rangle \) is the mean impact parameter.

The t-spectra, with \( t \approx (p_T^0)^2 \), are parametrized by

\[
\frac{dN}{dt} = A e^{-Bt}[1 + c(R(t) - 1)]
\]

(6)

where \( R(t) \equiv [dN / dt]_{\text{int}} / [dN / dt]_{\text{noint}} \) is the ratio of the t-distributions with and without interference obtained from Monte-Carlo simulations based on the KN model \[11\]. A is the overall normalization, \( B \) the slope parameter for coherent \( \rho^0 \) production, and \( c \) measures the strength of the interference: \( c = 0 \) corresponds to no interference, whereas \( c = 1 \) is the expected interference in the KN model.

Figure 5. Efficiency-corrected t-spectra for (a) the minimum bias data set with |\( y_ρ \)| < 0.5 and for (b) the topology data set with 0.05 < |\( y_ρ \)| < 0.5. The minimum bias data exhibit a wider dip at low \( t \), because the median impact parameter is smaller. The solid line shows a fit to Eq. (6).

Due to the neutron tagging of mutual Coulomb excitation in the minimum bias trigger, the median impact parameter of \( \vec{b} \approx 18 \text{ fm} \) in this data set is smaller than the \( \vec{b} \approx 46 \text{ fm} \) in the topology data. Therefore the dip in the minimum bias t-spectra should extend to larger values of \( t \). Figure 5 shows the efficiency-corrected t-distributions for the run 2002 topology and minimum bias data sets from Au-Au collisions at \( \sqrt{s_{NN}} = 200 \text{ GeV} \) in the central rapidity region |\( y_ρ \)| < 0.5 together with a fit to Eq. (6). To avoid contamination of the topology sample by cosmic

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Table 1
Spin density matrix elements for coherent \( \rho^0 \) production accompanied by mutual Coulomb excitation in Au-Au collisions at \( \sqrt{s_{NN}} = 200 \text{ GeV} \) \[8\] compared to ZEUS results from \( \rho^0 \) production in \( \gamma p \) collisions \[10\].

| Parameter | STAR | ZEUS |
|-----------|------|------|
| \( r_{00}^{04} \) | \(-0.03 \pm 0.03_{\text{stat}} \pm 0.06_{\text{syst}} \) | \(0.01 \pm 0.01_{\text{stat}} \pm 0.02_{\text{syst}} \) |
| \( \Re[r_{10}^{04}] \) | \(- \) | \(0.01 \pm 0.01_{\text{stat}} \pm 0.01_{\text{syst}} \) |
| \( r_{11}^{04} \) | \(-0.01 \pm 0.03_{\text{stat}} \pm 0.05_{\text{syst}} \) | \(-0.01 \pm 0.01_{\text{stat}} \pm 0.01_{\text{syst}} \) |
rays, in addition the region \(|y_\rho| < 0.05\) was excluded.

The minimum bias data exhibit an interference strength of \(c = 0.92 \pm 0.07\) \(\text{stat.}\) close to the expected value. The value from the topology data set is lower with \(c = 0.73 \pm 0.10\) \(\text{stat.}\), but could be affected by the imperfect topology trigger simulation.

2.3. Incoherent \(\rho^0\) Production in Au-Au Collisions

The incoherent \(\rho^0\) production, where the \(\rho^0\) couples to the individual nucleons, can be measured by extending the analyzed range of the \(\rho^0\) transverse momentum to 550 MeV/c. If the region of \(t < 0.002\) (GeV/c)^2, where interference effects reduce the cross section (see subsection 2.2), is excluded, the \(t\)-distribution can be described by a double exponential function

\[
\frac{d\sigma}{dt} = A_{\text{coh}} e^{-B_{\text{coh}} t} + A_{\text{inc}} e^{-B_{\text{inc}} t} \tag{7}
\]

\(B_{\text{coh}}\) is the slope parameter of the exponential that dominates the low-\(p_T\) region and corresponds to the coherent production. Accordingly \(B_{\text{inc}}\) is the slope parameter of the incoherent production that extends to larger \(p_T\).

Figure 6 shows a fit of Eq. (7) to the year 2002 minimum bias data from Au-Au at \(\sqrt{s_{NN}} = 200\) GeV that gives \(B_{\text{coh}} = 388 \pm 24\) \(\text{stat.}\) (GeV/c)^{-2} and \(B_{\text{inc}} = 8.8 \pm 1.0\) \(\text{stat.}\) (GeV/c)^{-2} [8]. By integrating the exponentials the cross section ratio of incoherent to coherent \(\rho^0\) production accompanied by mutual Coulomb excitation was measured to \(29 \pm 3\) \(\text{stat.} \pm 8\) \(\text{syst.}\) %.

2.4. \(\rho^0\) Production in \(d\)-Au Collisions

In \(d\)-Au ultra-peripheral collisions the virtual photon is predominantly emitted by the gold nucleus, due to its larger charge. There are two possible \(\rho^0\) production processes: coherent scattering on the entire deuteron, \(\gamma^* d \rightarrow \rho^0 d\), and “incoherent” scattering on the individual nucleons of the deuteron in the course of which the deuteron dissociates, \(\gamma^* d \rightarrow \rho^0 n\).

During the year 2003 run STAR took data of \(d\)-Au collisions at \(\sqrt{s_{NN}} = 200\) GeV using two UPC triggers. The first trigger was a topology trigger which selected mainly coherent interactions. The second trigger required, in addition to the topology condition, a neutron signal from the deuteron breakup in the corresponding ZDC. This data sample contains incoherent scattering events.

Figure 7 shows the \(t\)-spectrum, with \(t \approx (p_T^d)^2\), for incoherent scattering accompanied by deuteron dissociation. A fit with an exponential gives a slope parameter of \(B = 9.1 \pm 0.9\) \(\text{stat.}\) (GeV/c)^{-2} which is related to the nucleon form factor. This value is compatible with the slope parameter of \(B_{\text{inc}} = 8.8 \pm 1.0\) \(\text{stat.}\) (GeV/c)^{-2} measured in incoherent \(\rho^0\) production accompanied by mutual Coulomb excitation in Au-Au collisions at \(\sqrt{s_{NN}} = 200\) GeV (cf. subsection 2.3) [8] and also agrees with the value of \(B = 10.9 \pm 0.3\) \(\text{stat.} +1.0\) \(\text{syst.}\) (GeV/c)^{-2} measured at ZEUS [10]. The downturn of the distribution at low \(t\), which is also seen in low energy \(\gamma d\) experiments [16], is due to the fact that there is not enough energy to dissociate the deuteron.
3. $e^+e^-$-Pair Production in Photon-Photon Interactions

During the year 2002 run STAR also measured the production of $e^+e^-$-pairs in photon-photon interactions in ultra-peripheral Au-Au collisions at $\sqrt{s_{NN}} = 200$ GeV [17]. Since the electromagnetic field is strong with $Z\alpha \approx 0.6$, one expects to see higher-order QED effects. In order to enrich collisions at small impact parameters, where the fields are strongest and thus higher-order corrections should be most pronounced, a ZDC trigger was employed, requiring mutual nuclear dissociation and thus limiting the impact parameter to $2R_A < b \lesssim 30$ fm.

In the offline analysis events were selected that had two reconstructed tracks of opposite charge emerging from a common (primary) vertex along the beamline. Up to two additional tracks, not associated to the primary vertex, were allowed in order to account for random backgrounds. Most of the $e^\pm$ are produced in forward direction with low transverse momentum, so that only a small fraction of the pairs reached the central detectors, even though the solenoid field was reduced to 0.25 T, half of its nominal value. The tracks were required to have pseudorapidities of $|\eta| < 1.15$ and transverse momenta of $65 < p_T < 130$ MeV/c. The latter cut ensured that the $e^\pm$ identification via the specific energy loss in the TPC gas had only minimal contaminations from other particle species. Additional cuts on the pair transverse momentum, $p_T^{e^+e^-} < 100$ MeV/c, and the pair rapidity, $|y_{e^+e^-}| < 1.15$, gave a final sample of 52 events in the pair invariant mass region of $140 < M_{e^+e^-} < 265$ MeV/c$^2$.

The measured cross section in the selected kinematic range is $1.6 \pm 0.2_{\text{stat.}} \pm 0.3_{\text{syst.}}$ mb. Figure 8 shows the cross section as a function of the transverse momentum of the $e^+e^-$-pair, Fig. 8b the pair invariant mass distribution. The data are compared to a a recent QED calculation of Baltz that includes a realistic phenomenological treatment of the nuclear Coulomb excitation [18]. The lowest order QED (dashed line in Fig. 8) overpredicts the data. The calculated cross section of 2.34 mb is nearly 2 standard deviations above the data. The corresponding higher-order QED calculation gives a cross section value of 1.67 mb, compatible with the measurement, and also describes the kinematic distributions well.

4. Coherent Photonic $\pi^+\pi^-\pi^+\pi^-$ Production

During the year 2004 run STAR took data in Au-Au collisions at $\sqrt{s_{NN}} = 200$ GeV using a “multi-prong” trigger which combined the UPC neutron tag in form of coincident ZDC signals
with a low hit multiplicity in the CTB. In addition a veto from the large-tile Beam-Beam Counters (BBCs) [19], which cover $2.1 < |\eta| < 3.6$, was applied.

Events were selected that have four charged tracks coming from one common (primary) vertex. These four-prongs were required to be neutral and to have a net transverse momentum below 150 MeV/c, thus selecting coherent production. A low number of additional tracks, unassociated to the primary vertex, were allowed in the events to account for backgrounds.

The transverse momentum distribution of the neutral four-prongs in Fig. 9a shows the expected peak at low $p_T$, characteristic for coherent production. The $\pi^+\pi^-\pi^+\pi^-$ invariant mass spectrum in Fig. 9b shows a broad peak of approximately 100 events around 1510 MeV/c^2 which could be caused by the production of excited $\rho^0$ states like the $\rho^0(1450)$ and/or the $\rho^0(1700)$.

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