Multiple Electron Acceleration Instances during a Series of Solar Microflares Observed Simultaneously at X-Rays and Microwaves

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Abstract

Even small solar flares can display a surprising level of complexity regarding their morphology and temporal evolution. Many of their properties, such as energy release and electron acceleration can be studied using highly complementary observations at X-ray and radio wavelengths. We present X-ray observations from the Reuven Ramaty High Energy Solar Spectroscopic Imager and radio observations from the Karl G. Jansky Very Large Array (VLA) of a series of GOES A3.4–B1.6 class flares observed on 2013 April 23. The flares, as seen in X-ray and extreme ultraviolet, originated from multiple locations within active region NOAA 11726. A veritable zoo of different radio emissions between 1 GHz and 2 GHz was observed cotemporally with the X-ray flares. In addition to broadband continuum emission, broadband short-lived bursts and narrowband spikes, indicative of accelerated electrons, were observed. However, these sources were located up to 150'' away from the flaring X-ray sources but only some of these emissions could be explained as signatures of electrons that were accelerated near the main flare site. For other sources, no obvious magnetic connection to the main flare site could be found. These emissions likely originate from secondary acceleration sites triggered by the flare, but may be due to reconnection and acceleration completely unrelated to the cotemporally observed flare. Thanks to the extremely high sensitivity of the VLA, not achieved with current X-ray instrumentation, it is shown that particle acceleration happens frequently and at multiple locations within a flaring active region.

\textit{Unified Astronomy Thesaurus concepts:} The Sun (1693); Solar radio flares (1342); Solar flares (1496); Solar x-ray flares (1816); Solar activity (1475)

1. Introduction

Solar flares are magnetic energy release events in the solar atmosphere that efficiently accelerate particles to relativistic speeds. The most direct signatures of flare accelerated electrons are found at X-ray and radio wavelengths. Observations at these wavelengths are highly complementary (e.g., White et al. 2011) and allow us to diagnose the locations and mechanisms of particle acceleration in solar flares and to study how particles are transported close to the Sun and away from the Sun.

Gyrosynchrotron emission at frequencies above \(\sim 2 \text{GHz}\) and X-ray emission at a few tens of keV originating from high energetic, nonthermal electrons are often found to be tightly correlated (e.g., Melnikov et al. 2002; Krucker et al. 2010). In a statistical study on the timings of X-ray and radio emission at 17 GHz and 34 GHz, Krucker et al. (2020) found that this may in fact hold for the majority of larger flares. In single-event analysis, such a common origin of the emissions leads to a more complete scenario of electron acceleration than observations at one wavelength alone (e.g., Gary et al. 2018). Chen et al. (2021) performed an in-depth study of a source above the top of magnetic loops (above-the-loop-top source). Such sources have been interpreted as the (primary) acceleration site (e.g., Masuda et al. 1994; Krucker et al. 2010; Chen & Petrosian 2012; Krucker & Battaglia 2014; Battaglia et al. 2019). Combining spatially resolved X-ray and radio spectra, Chen et al. (2021) inferred the energetic electron spectrum at the acceleration site over a much wider energy range than would be possible from observations at either wavelength alone.

However, very often, radio emission is not observed from the same location as X-rays. This is typically the case for different types of coherent emission observed below \(\sim 2 \text{GHz}\). In many instances, such emission is due to beams of accelerated electrons whose X-ray signatures are too faint to be detected with current instrumentation (e.g., Saint-Hilaire et al. 2009; Chen et al. 2018; Glesener & Fleishman 2018), that are propagating away from the Sun on open field lines. In many of these cases it is found that the electrons were accelerated at the same site as electrons that become trapped in closed magnetic loops. However, a number of authors found such emissions to originate from a different, secondary acceleration site (e.g., Battaglia & Benz 2009; Benz et al. 2011; Carley et al. 2016; Chen et al. 2015, 2019). Large solar flares usually have a long duration (up to several hours) and often display a complex morphology with multiple loop systems, hence it is not surprising that multiple acceleration sites are found. However, even smaller flares, so-called microflares (Hannah et al. 2011) can display a remarkable complexity as demonstrated by, e.g., Sharma et al. (2020), Glesener et al. (2020), Duncan et al. (2021), and Vievering et al. (2021). Understanding this complexity and different features observed at both radio and X-ray wavelengths is the key to understanding where and how electron acceleration takes place and how electrons are transported.

Here, we present a series of microflares, ranging in GOES class from B8 to B9.3 (A3.4 to B1.6 background subtracted) that were observed simultaneously at X-rays by the Reuven Ramaty High Energy Solar Spectroscopic Imager (RHESSI; Lin et al. 2002), at radio frequencies between 1 GHz and 2 GHz by
the Karl G. Jansky Very Large Array (VLA, Perley et al. 2011), and at extreme ultraviolet (EUV) wavelengths by the Atmospheric Imaging Assembly (AIA; Lemen et al. 2012) on board the Solar Dynamics Observatory (SDO; Pesnell et al. 2012). The flares happened on 2013 April 23 over a duration of 50 minutes. They all originated from active region NOAA 11726 (N13W49) but from different locations within it. During the observations, a veritable zoo of different radio emissions was observed, most, but not all, temporally associated with X-ray flares. However, there was no spatial association between the radio emissions and the X-ray flare locations, suggesting multiple acceleration instances and sites before, during, and after the main flares, and energetic particles that gained access to large or open field lines far away from the main acceleration site. This work is intended as an overview of all events, representing the “bigger picture.” Individual events will be analyzed in-depth in a follow-up publication.

In Section 2 an overview of the active region, the X-ray flares, and radio emissions is given, followed by a detailed description of imaging and spectral analysis in both X-rays and radio wavelengths (Section 3). In Section 4, a detailed investigation of the temporal and spatial association between radio emissions and X-ray emission in the different flares is made. The findings are discussed and interpreted in Section 5. Conclusions are drawn in Section 6.

2. Event Overview

The flares were observed on 2013 April 23 between 20:10 UT and 21:00 UT. Figure 1 shows the median radio cross-power dynamic spectrum between 1 and 2 GHz along with the GOES 1–8 Å lightcurve and RHESSI X-ray lightcurves at two energy bands (4–8 keV and 10–18 keV). Seven individual flares were identified based on X-ray emission in the RHESSI 10–18 keV lightcurves, the highest photon energies that RHESSI detected from these flares. The individual flares were numbered 1–7, as indicated in the figure. We will refer to them as F1 through F7. The corresponding radio sources will be denoted F1R through F7R. For all flares, except F3 and F4, the intensity at 10–18 keV returned to background level between each flare. Since X-ray images of F4 showed an additional source, not visible during F3, these two peaks were treated as individual flares rather than one flare with two peaks. The 10–18 keV emission of all flares except F1 is quite impulsive, suggesting potential nonthermal emission while the lightcurve of F1 is more gradual in both energy ranges, hinting at purely thermal emission. A definite distinction is only possible through spectroscopy (see Section 3.1).

During the whole duration of the observations, various types of radio emissions were visible in the dynamic spectrum: broadband continuum emission above 1.5 GHz, most prominently during F3–F7, broadband short-lived bursts during F5–F6, and narrowband spikes in the decay phase of F6. The latter two will be referred to as F60R and F68R. Even though these emissions were temporally associated with the X-ray flares, there was no clear time correlation. Table 1 gives a summary of the observed features, including the X-ray peak times, the time integrations of the RHESSI and VLA images (see Section 3) and a short description of the observed features in the radio dynamic spectrum.

3. Data Analysis

X-ray images and spectra were generated at the high-energy X-ray peak time of each of the seven flares. Radio images and spectra were generated at the same times as the X-ray data products. Additionally, images and spectra of the burst and the spikes in the decay phase of F6 were generated, as described in detail below.

3.1. X-Ray Imaging and Spectroscopy

RHESSI images were generated using the CLEAN algorithm (Högbom 1974; Hurford et al. 2002) for two energy bands: 4–8 keV (thermal emission) and 10–18 keV (potentially nonthermal emission). For the image reconstruction, detectors 5, 6, 7, and 8 were chosen to limit noise contributed by detectors with finer grids either because there was no flux modulation or because of reduced detector sensitivity during that time of the mission. The image integration time was chosen to include the whole high-energy peak but minimum 60 s to achieve good count statistics, especially in the higher energy band. The image integration times are listed in Table 1. X-ray spectra were generated using the same integration times as for the images. For spectral fitting, detector 6 was used because, at that point in the RHESSI mission, this detector had the highest sensitivity with relatively low background. All flares were fitted with a single thermal component at the lowest energies (compare Table 2). However, spectral fitting of the higher energies proved difficult. After careful background subtraction, only a few counts were observed at energies between 10 and 18 keV, most prominently in F4 and F7. Since detector pileup could be excluded as the origin of this emission, we interpreted it as weak signatures of accelerated, nonthermal electrons and took the following approach to obtain an upper limit on the nonthermal electron spectrum. The single thermal component fitted previously was fixed and an additional nonthermal thick-target component was fitted up to ~18 keV, depending on the flare. Then both the thermal and nonthermal components were fitted simultaneously. Even though a nonthermal component could be fitted in this manner, the parameters were not well constrained with uncertainties that were larger than the fit parameters in many cases. An example spectrum is given in Figure 2. The nonthermal spectrum shown in the figure corresponds to a total electron flux of $F_e = 1.0 \times 10^{-3}$ s$^{-1}$, an electron spectral index $\delta = 4.9$, and a low-energy cutoff $E_{\text{low}} = 6.5$ and has to be seen as an upper limit. An additional difficulty was posed by F1 and F4 for which two X-ray sources could be imaged simultaneously. Hence, these flares were actually constituted of two separate events happening simultaneously and the full Sun spectra are superpositions of both. For larger flares, individual spectra of flaring sources can be isolated through imaging spectroscopy (e.g., Emslie et al. 2003; Battaglia & Benz 2006; Simões & Kontar 2013; Krucker & Battaglia 2014). However, the sources here were too faint to be imaged at more than two energy bands. Note that a fitting model consisting of two purely thermal components with different temperatures would be another possibility. Such a model resulted in even larger uncertainties of the fit parameters and was discarded.

3.2. Radio Imaging and Spectroscopy

The VLA observations (under the observing program VLA/13A-384) were carried out using two subarrays. One subarray...
observed in the 1–2 GHz (\(\lambda = 15–30\) cm) L band with 13 antennas, and another in the 2–4 GHz (\(\lambda = 7.5–15\) cm) S band with 13 antennas. In the present study, we focus on the 1–2 GHz L-band data where the radio bursts are present. The L-band data had a spectral resolution of 2 MHz and temporal resolution of 50 ms in both the right-hand- and left-hand-circular polarizations (RCP and LCP). The spectral range of the observations was divided uniformly into eight spectral windows. Each spectral window had 64 2 MHz wide frequency channels. The L-band subarray was in D-configuration with a total of 13 antennas used for the observations. The longest baseline was 1031 m, corresponding to an angular resolution of 70\(''\) \times 40\(''\) at 1.5 GHz at the time of the observations.

CLEAN images in both RCP and LCP were made during the X-ray peak time of each flare and, additionally, for the burst and the spikes in the decay phase of F6. A time integration of 1 second and frequency integration of 20 MHz were used for all images except the spikes. The latter were only detected at the lowest frequencies, extremely short-lived and much brighter than the other sources. Hence, they were imaged at full time resolution of 50 ms and full frequency resolution of 2 MHz. A circular beam with FWHM of 70\(''\) at 1 GHz, linearly decreasing to 40\(''\) at 2 GHz, was used for image convolution. The radio emission observed in the dynamic spectrum was dominated by background emission of the active region that acted as a strong background source. Hence, background subtraction was performed in the visibility domain to isolate the flaring sources. As background time, the time interval between 20:08:00 and 20:08:01 UT was chosen (20:45:24.5-20:45:25.0 UT for F6s). Figure 2 shows images of the background source and the burst in LCP during F6 at selected frequencies for comparison. The centroid location of the burst sources was determined as a function of frequency by fitting a 2D Gaussian at a flux level of >90% of the maximum emission in each image. Radio spectra were computed from the brightness temperature maps by selecting the maximum brightness temperature of the source in images for which a source location could be fitted. At some frequencies the images were dominated by noise and no

![Figure 1](image-url)

**Figure 1.** Panel (A): VLA median cross-power dynamic spectrum between 1 GHz and 2 GHz. The orange and red lines are the RHESSI 4–8 keV and 10–18 keV lightcurves, respectively (arbitrary scaling). Flares were identified as individual peaks in the 10–18 keV lightcurve and labeled 1–7. The GOES lightcurve at 1–8 Å is given in dark gray (axis on the right-hand side). Panel (B): X-ray lightcurves as in panel (A). Additionally, the frequency integrated radio lightcurve is given as blue line. Panel (C): inset between 20:45:25 UT and 20:45:45 UT, showing narrowband spikes in the decay phase of F6.
Table 1
X-Ray Peak Times in the 10–18 keV Lightcurve, X-Ray Image Integration Time, Radio Feature Identified in Dynamic Spectrum, and Radio Image Integration Times

| Flare No. | X-Ray Peak-time (UT) | X-Ray Integration Time (UT) | Dominant Radio Feature in Dynamic Spectra | Radio Image Integration Time |
|-----------|----------------------|-----------------------------|------------------------------------------|----------------------------|
| 1         | 20:17:42             | 20:15:00-20:19:30           | no VLA data                              | ...                        |
| 2         | 20:26:10             | 20:27:10-20:29:10           | broadband continuum                      | 20:26:41.5-20:26:42.5     |
| 3         | 20:34:25             | 20:33:30-20:35:36           | broadband continuum                      | 20:34:30-20:34:31         |
| 4         | 20:36:47             | 20:35:40-20:38:36           | short-lived burst                         | 20:37:31-20:37:32         |
| 5         | 20:40:51             | 20:40:00-20:42:36           | none                                     | 20:40:54-20:40:55         |
| 6         | 20:44:31             | 20:43:50-20:46:02           | short-lived burst during decay phase      | 20:44:30-20:44:31         |
| 6b        | 20:44:31             |                             | narrow-band spikes during decay phase    | 20:45:21-20:45:22         |
| 6 s       | 20:44:31             |                             | none                                     | 20:45:25.90-20:45:25.95   |
| 7         | 20:56:04             | 20:55:20-20:57:00           | none                                     | 20:56:05.5-20:56:06.5     |

Table 2
Temperature and Emission Measure from X-Ray Spectral Fitting

| Flare No. | Emission Measure (10^6 cm^-3) | Temperature (MK) |
|-----------|-------------------------------|------------------|
| 1         | 4.1 ± 0.3                     | 10.7 ± 0.1       |
| 2         | 4.5 ± 0.5                     | 10.0 ± 0.2       |
| 3         | 3.5 ± 0.3                     | 11.4 ± 0.1       |
| 4         | 1.3 ± 0.9                     | 14.3 ± 1.7       |
| 5         | 1.3 ± 0.9                     | 14.3 ± 1.7       |
| 6         | 1.7 ± 0.1                     | 12.6 ± 0.2       |
| 7         | 1.2 ± 1.8                     | 11.5 ± 0.7       |

3.3. EUV and Magnetic Field Imaging

AIA images and magnetic field maps from the Helioseismic and Magnetic Imager (HMI; Scherrer et al. 2012) on SDO were processed using the standard data processing pipeline for these instruments. Using the method developed by Del Zanna (2013), we also constructed AIA maps of the Fe XVIII line, which has a peak formation temperature of 8 MK (Del Zanna et al. 2015), typical for smaller flares.

4. Results

First, we investigate the X-ray location of each flare relative to the other flares and to flaring emission seen at EUV wavelengths and an HMI magnetogram, followed by presentation of the radio source locations relative to each other and to the X-ray sources and EUV emission features.

4.1. X-Ray Source Locations

Figure 3 summarizes the locations of the X-ray flares relative to features in AIA 171 Å and Fe XVIII images and an HMI magnetogram. The AIA images were composed by averaging images at 20:27:01 UT, 20:45:01 UT, and 20:54:59 UT. The AIA 171 Å wavelength band is most sensitive to cooler plasma around 1 MK while the Fe XVIII images show plasma at 8 MK. The locations of the X-ray sources at 4–8 keV are given as contour levels relative to the maximum in each image on the AIA image and as symbols on the HMI image. The magnetogram shows a complex magnetic topology with large positive and negative polarity patches at either side of the active region, interspersed with smaller patches of either polarity. EUV images show multiple loops at different temperatures. A large loop system, best visible in Fe XVIII images, seems to connect the large positive and negative magnetic field patches. Smaller loops are visible between the large loops. X-ray and radio images show sources from multiple locations within the active region over the 50 minutes of observations. F1 and F2 originated from the base of a larger loop system, visible at 171 Å and where associated with an EUV jet. There was a second, fainter source imaged during F1 that was associated with a different loop system seen in the Fe XVIII images. F3–F6 originated from a small loop system, clearly visible in the Fe XVIII images but not at the same location as F1 and F2. An additional, fainter source was observed during F4 that had no such obvious EUV counterpart. F7 originated from yet another location, close to the footpoint of an EUV loop.

4.2. Radio Source Locations

Figure 3 gives the frequency-averaged centroid locations of the radio sources during each X-ray flare. The error bars give the 1σ standard deviation, representing the frequency-dependent scatter of the sources. All radio sources were located eastward of the hot EUV loops and the locations with strongest magnetic field. None of them were cospatial with any of the X-ray sources or with the EUV loops.

For the brightest radio features (F5R, F6bR, and F6sR) we also investigate the locations as a function of frequency. These are shown in Figure 4, overlaid on a composite AIA image and individually over AIA 171 Å images. The color table in the EUV images was adapted such that faint loops become more visible. For F5R and F6bR we restricted ourselves to centroid locations for which the maximum flux of the source was larger than 0.3 MK. As mentioned before, none of these sources coincide with any of the X-ray sources. F5R shows a systematic displacement of the centroid location as a function of frequency perpendicular to a large, faint loop visible at 171 Å. F6bR and F6sR originate from about the same location, close to a fan-like structure. The scatter of the frequency-dependent centroids in F6bR is considerable and there is no clear trend, other than that lower frequencies seem to originate preferentially further north than higher frequencies. Within F6sR, the scatter is smaller than
in F6bR, but again no systematic displacement of the locations as a function of frequency can be observed.

4.3. Spectra

4.3.1. X-Ray Spectra

Table 2 summarizes the results from the thermal spectral fitting as described in Section 3.1. As an example of a fitted spectrum, Figure 2 shows the background-subtracted count rate spectrum of F4. The background-subtracted count rate above 10 keV was around the background level, yet two sources could be imaged in this energy range. The temperatures of the flares ranged between 10.0 MK in F2 and 14.3 MK in F4 and F5. The emission measure was lowest in F7 at 1.2 × 10^{46} cm$^{-3}$ and highest in F2 at 4.2 × 10^{46} cm$^{-3}$. Even though a nonthermal component could be fitted in F4 and F7, the uncertainties were too large (same order or larger as the fit parameters) for the result to be interpreted with confidence.

4.3.2. Radio Spectra

The radio spectra shown in Figure 2 show the maximum brightness temperature as a function of frequency in LCP polarization. Except for F5R, F6sR, and F6bR the brightness temperature was low (less than ~0.5 MK) or, depending on the frequency, at the noise level of the image. Emission during F5R was detected at almost all frequencies and peaked at ~1.4 GHz. F6bR had the highest brightness temperature among the broadband features with a maximum around 2.1 MK at 1 GHz, declining to 0.3 MK at 2 GHz. The maximum brightness temperature of F6sR (spikes) was 5 MK. Since such bursts may originate from fairly compact source regions, it is likely that they are not spatially resolved. Indeed, the FWHM of the fitted 2D Gaussian was around 20″ at 1.1 GHz, while the restoring beam size was 60″. Hence these values should be considered as lower limits.

5. Discussion

During a 50 minute time window, seven X-ray flares between GOES A3.4 and B1.6 (background subtracted) were observed cotemporally with a variety of radio emissions, such as broadband bursts, narrowband short-lived spikes, and broadband continuum emission at frequencies between 1 to 2 GHz. The broadband continuum emission can be attributed to background thermal emission of the active region, while the short-lived bursts and spikes are indicative of accelerated electrons. The X-ray flares displayed quite typical characteristics regarding size, spatial origin, and energies, as will be discussed in more detail in Section 5.1. The radio sources were displaced from the X-ray sources by more than 100″ despite close temporal association with the X-ray emission. In
Section 5.2 we will discuss possible explanations for this displacement.

5.1. X-Ray Microflare Locations and Energies

The observed microflares were quite ordinary in the sense that they were short and compact. It is noteworthy that, during F1–F4, two sources from different locations within the active region were imaged. Since the RHESSI imaging technique favors the brightest source present, this means both of these sources were of comparable brightness and the X-ray light-curves and spectra consist of a superposition of emission from two separate flares that were, however, too faint to be analyzed individually through imaging spectroscopy.

X-ray spectra indicate emission up to $\sim$14 keV. For all flares it was possible to fit a thermal component. From the fitted temperature $T$ and emission measure $EM$ one can calculate the thermal energy as

$$E_{\text{th}} = 3k_B T \sqrt{EM \times V},$$

where $k_B$ is the Boltzmann constant and $V$ is the flaring volume. Assuming a filling factor of unity and a flaring volume of $V = A^{3/2}$, where $A$ is the area of a circle of radius $10''$, one finds thermal energies of the order of $2.4 \times 10^{28}$ erg to $4 \times 10^{28}$ erg. Emission above $\sim$10 keV was at the background level and any spectral fitting model was not well constrained, as described in Section 3.1. Using upper limit spectral parameters (total electron flux $F_e = 1.0 \times 10^{34}$ s$^{-1}$, electron spectral index $\delta = 4.9$, and low-energy cutoff $E_{\text{low}} = 6.5$ keV) the total nonthermal power is calculated as

$$P = \frac{\delta - 1}{\delta - 2} F_e E_{\text{low}} = 1.4 \times 10^{26} \text{ erg s}^{-1}.$$  

Both thermal and nonthermal energies are consistent with earlier findings using RHESSI observations for similarly sized flares (Stoiser et al. 2007; Hannah et al. 2008; Inglis & Christe 2014).

Figure 3. Top row: locations of X-ray sources at 4–8 keV relative to EUV emission in the Fe XVIII line (left) and an HMI magnetogram (right). On the AIA FFe XVIII image the X-ray sources are indicated by the 50%, 70%, and 90% contours of RHESSI CLEAN. Numbers next to the sources give the flare number according to the legend on the right. On the right, the location of maximum emission in RHESSI images is indicated by crosses. Here, the location of weaker X-ray sources during F1 and F4 are also indicated near coordinates [650,300] and [680,260], respectively. Different symbols are used for better visibility with arbitrary symbol size. The starting times of the RHESSI images are given to the right in the respective colors along with the flare number. Bottom row: AIA 171 Å image and HMI image overlaid with the frequency-averaged location of the radio sources associated with each flare. The size of the cross gives the standard deviation of the frequency-dependent source locations. For better visibility, the location and standard deviation of the spike locations is indicated with an ellipse. The locations of F6bR and F6sR are marked, respectively.

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![Image of X-ray sources](image-url)
5.2. Radio Sources as Secondary Acceleration Sites?

The most noteworthy observation is the significant displacement between the location of the radio burst sources and the X-ray sources. In a simple scenario in which electrons are accelerated during a flare and the signatures of the same accelerated electron population are observed at both X-ray and radio wavelengths one would expect the locations of the radio sources to be close to the flaring site as seen in X-rays where the radio emission can be either gyrosynchrotron emission from electrons trapped in flaring loops or coherent emission from electron beams escaping along open field lines visible as, e.g., type III bursts. However, only some of the observations presented here can be explained with this simplest scenario.

Observationally one can distinguish three cases:

1. Both X-ray and radio sources originate from the same magnetic loop structure (F7).
2. Radio emission does not originate from the same magnetic structure as X-ray emission, but both structures are magnetically connected (F4, F5).
3. Radio emission originates from a different magnetic structure seemingly not connected to the original X-ray flare site (F6).

To investigate the magnetic connectivity of the active region and confirm the cases outlined above, we performed nonlinear force free magnetic field extrapolations (NLFFF) using the gx_simulator package (part of the IDL SolarSoftware distribution; Nita et al. 2015), shown in Figure 5. The extrapolations show four major structures: small, closed magnetic loops at the western side of the active region (labeled W in Figure 5); large, open and closed field lines in the north (N); a closed loop structure centered between the two mentioned before (C), and another, separate structure to the east (E). Except for the last one, the magnetic loops found by the NLFFF are also visible at EUV wavelengths. Due to projection effects it is difficult to locate the sources on the magnetic field model exactly and the available data do not provide enough constraints to locate them based on density or height arguments, hence, the likely locations are indicated with elliptic shapes in the figure, where white ellipses outline the most likely origin of the X-ray emission and purple shapes indicate the likely origin of the corresponding radio emission deduced by qualitative comparison of the EUV features and radio and X-ray source locations. In the following we provide some physical scenarios and explanations for the cases listed above.

5.2.1. Scenario 1: Same Electron Population within Same Magnetic Loop (F7)

During F7, radio emission was observed cotemporally with X-ray emission and, as can be seen in Figures 4 and 5, the sources at the two different wavelengths originated from the same magnetic loop structure. These observations are compatible with a scenario in which electrons are accelerated during a flare, become trapped in a closed magnetic loop and emit radiation at X-ray and radio wavelengths.

5.2.2. Scenario 2: Same Electron Accelerated Electron Population with Significant Transport (F4, F5)

The radio emission in both of these events was observed cotemporarily with the high-energy X-ray emission with the strong burst in F5R happening 3 s after the X-ray peak. The frequency-dependent locations of F5R show no clear trend, indicating that the electrons do not propagate away from the Sun along open field lines as, in that case, one would expect a clear frequency dependence of the source location (e.g., Chen et al. 2013, 2018). For both of these cases it is likely that the emission is due to electrons that were accelerated near location W and were either directly injected into one of the field lines of loop system C or gained access to it through cross-field diffusion.

5.2.3. Scenario 3: Secondary Electron Acceleration (F6b, F6s)

Both F6bR and F6sR happened between 50 s and 54 s after the X-ray peak time, and originated from field lines that seemingly are not connected to the X-ray flare site. Short-lived spikes, similar to F6sR, at MHz to GHz frequencies have commonly been interpreted as signatures of flare accelerated electrons due to their high temporal association with hard X-rays (e.g., Benz 1986; Guedel et al. 1991; Aschwanden & Guedel 1992).
However, imaging studies of spikes showed that they can be displaced as much as $400\arcsec$ from the main flare site (Benz et al. 2002; Khan & Aurass 2006; Battaglia & Benz 2009). Such findings suggested that spikes are signatures of secondary acceleration that typically happen higher in the corona but are causally linked to the main energy release. However, the connection to the main energy release is not always obvious. Recently, Luo et al. (2021) observed a stochastic spike burst associated with an M-class flare for which the connection with the flare was not obvious as is the case for F6$eta$ and F6$eta$$e$ in the observations presented here.

Since the NLFFF extrapolated field may deviate from the actual magnetic connectivity in the corona, particularly during flaring times, one explanation is that we do not capture the field lines that connect regions W and E and electrons were accelerated during the flare in region W and transported to region E, similar to the second scenario. However, a more intriguing explanation is that electrons were accelerated in situ at a secondary acceleration site, triggered by the original flare. Such sympathetic flares, but also coronal mass ejections, filament eruptions, and solar energetic electron events have been known for quite some time (e.g., Pearce & Harrison 1990; Wang et al. 2018, 2021), and have been found to even happen between active regions. The exact mechanism that causes them is still under debate. It has been suggested that the regions involved could be connected by large-scale coronal loops (e.g., Wang et al. 2001; Jiang et al. 2008) that are perturbed but the original flare which results in reconnection events far away from the original flare site.

6. Conclusions

The combined radio and X-ray observations shown here demonstrate that even smaller flares can display a surprising level of complexity. Despite close temporal association between radio and X-ray emission, the two types of emissions originated from entirely different regions. While for some events it can be argued, based on magnetic connectivity, that electrons were accelerated during the primary energy release, in the other events, the radio emissions are likely due to secondary energy release and particle acceleration, either completely unrelated to the primary energy release or triggered by it in a way yet to be understood. Thanks to the high sensitivity of the VLA it is shown that nonthermal processes happen frequently and at many different locations of an active region. Observations from future X-ray instruments that use focusing optics, resulting in a much higher sensitivity and dynamic range as current instruments, combined with VLA observations are needed to fully understand these processes.

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