Integrated petrophysical study to validate water saturation from well logs in Bahariya Shaley Sand Reservoirs, case study from Abu Gharadig Basin, Egypt

Mohamed El-Bagoury

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Abstract
Water saturation is a key parameter in evaluating oil and gas reservoirs and calculating OIIP and GIIP for petroleum fields. The late Cretaceous Bahariya reservoir contains variable amounts of clay minerals. Bore hole logs are affected with those clay minerals particularly the density and resistivity logs. Several methods are acknowledged to determine the true water saturation from well logs in shaley sand reservoirs. Each method assumes a sort of corrections to amount of shale distributed in the reservoir. The scope of this petrophysical study is to integrate core analysis and bore hole logs to investigate the characteristics of water saturation in the Bahariya reservoirs. Comparison between most of the significant shaley sand methods is presented in this research. Reservoir lithology and mineralogy are explained by Elan-model while bore hole images are used for fine-tuning the electrofacies. Siltstone, shaley sand and clean sandstones are the main electrofacies that is characterizing the Bahariya reservoir rocks. For accurate saturation results, some core samples have been used for validating the log-derived water saturation. Dean stark and cation exchange capacity experiments are integrated with bore hole logs to calculate the error in water saturation for each method for best calibration. The successful integration between logs and core measurements led to convenient log evaluation and accurate understanding for the Bahariya reservoir in the prospective part of Abu Gharadig basin.

Keywords Water saturation · Bahariya · Well logs · Electrofacies · Mineralogy · CEC

Abbreviations

| Abbreviation | Definition |
|--------------|------------|
| a            | Constant multiplier (unitless) |
| B            | Equivalent cationic conductance of a sodium ion (L S/m) |
| BHI          | Bore hole image |
| BVH          | Bulk volume of hydrocarbon (hydrocarbon pore volume) (fraction) |
| BVW          | Bulk volume of water (water pore volume) (fraction) |
| CEC          | Cation exchange capacity measured in lap (S/m) |
| CEC*         | Cation exchange capacity calculated from logs (S/m) |
| F            | Formation factor (unitless) |
| Gr_min       | Gamma ray minimum (API) |
| Gr_max       | Gamma ray maximum (API) |
| LR_p         | Low resistivity pay |
| m            | Cementation factor (unitless) |
| m*           | Modified cementation factor (non-Archie) (unitless) |
| n            | Saturation exponent (unitless) |
| n*           | Modified saturation exponent (non-Archie) (unitless) |
| Q_v          | Cation exchange capacity volumetric (Unite per liter) |
| R_t          | True (deep) resistivity in the un-invaded zone (Ohm-m) |
| R_s          | Shallow resistivity in the invaded zone (Ohm-m) |
| R_sh         | Resistivity of shale (Ohm-m) |
| S_w          | Un-invaded zone water saturation (%) |
| S_h          | Un-invaded zone hydrocarbon saturation (%) |
| R_w          | Formation water resistivity (Ohm-m) |
| R_v          | Vertical resistivity (Ohm-m) |
| R_h          | Horizontal resistivity (Ohm-m) |
| V_sh         | Volume of shale (fraction) |
| Φ_e          | Effective porosity (fraction) |
| ϱ_b          | Bulk density (g/cm³) |
| ϱ_ma         | Matrix density (g/cm³) |
| ϱ_f          | Fluid density (g/cm³) |

Mohamed El-Bagoury
M.el-Bagoury@Bapetco.net

1 Petroleum Engineering Department, Badr El-Din Petroleum Company, Cairo, Egypt
\( \Delta T_{\text{ma}} \) Matrix transit time (\( \mu s/\text{ft} \))
\( \Delta T_f \) Fluid transit time (\( \mu s/\text{ft} \))

**Introduction**

Petrophysical parameters as volume of shale (\( V_{sh} \)), porosity (\( \Phi \)) and water saturation (\( S_w \)) are generally used to evaluate the potential of hydrocarbon-bearing formations. In clean formations, water saturation can be calculated using the simple conductivity model of Archie’s equation, while in shaley sand reservoirs the clay minerals are bringing extra conductivity, which may bias the computed water saturation.

Shaley sand models were presented in North America during the Fifties by Hill and Milburn’s (1955) and their work led to cation exchange capacity concept by Waxman and Smits (1968). The problem of identifying low resistivity pay through wire line logs has been acknowledged with much early focus on Texas and Louisiana gulf coast (Tixier et al. 1968; Murphy and Owens 1972). Several models discussed the true water saturation in shaley sands as Simandoux (1963) and modified Simandoux equation by Bardon and Pied (1969), Indonesia and modified Indonesia formula by Poupon and Leveaux (1971), Juhasz (1981), Bassiouni (1994) and Iheanacho (2014). This present work aims to discuss different methods in calculating water saturation from bore hole logs which will be compared to values measured from core samples.

Bahariya formation is one of the shaley sand reservoirs that contain variable amounts of clay minerals (Abu Shady et al. 2010); those clay minerals which affect the pore system challenged the simple water saturation approaches (Shedid and Saad 2017). Bahariya mineralogy was investigated in Western Desert fields by many authors Hegazy and Labib (1996), Wehr et al. (2002), Abu Shady et al. (2010), El Sayed and El Sayed (2015), Shokry et al. (2015). The hydrocarbons potentiality of the late Cretaceous Bahariya Formation was proven in Abu Gharadig basin as 90% of Western Desert fields was producing from it (EGPC 1992).

**Formation evaluation technique** is connected to the amount and type of clays in pore system. The present work aims to discuss the clay minerals characterization using bore hole logs and extra conductivity known as cation exchange capacity (CEC) for one of the widely distributed reservoirs in Abu Gharadig basin and Western Desert (Fig. 1).

The study area is located in the easternmost part of Abu Gharadig basin some 150 km west of Cairo the capital of Egypt and about 100 km from Mediterranean Sea coast northeast of the inverted Mubarak Ridge (Fig. 1). The petrophysical data used in this work are obtained from the two oil fields Neag-1 and Neag-2, which were discovered at 2007/2008 by SHELL and currently operated by BAPETCO.

The Neag-1 field was investigated before by many authors (Bakr et al. 2010; ElBelisy et al. 2010; El-Bagoury et al. 2017; El-Bagoury 2019; El Sayed et al. 2019). Fit for purpose reservoir modeling for the geological uncertainties as., structure and stratigraphy was done for Bahariya reservoirs (Fault block compartmentalization, Fault sealing, sub-seismic faults, net reservoir, hydrocarbon saturation) by Bakr et al. (2010) to propose a fast track strategy for early field development. The key petrophysical parameters and its related uncertainties were adjusted by ElBelisy et al. (2010) via integrating the core photographs and bore hole logs to fine-tune the net reservoir cutoffs initially selected based on other analogues. This was mainly effective in approximating the in place volumes which enhanced after shaley sand trials. The number of segments and zones was increased by El-Bagoury et al. (2017) to achieve detailed modeling for Bahariya reservoir in order to match the production and pressure history of the field. This approach enhanced the geologic and engineering understanding of Neag-1 field for best water flood pattern selection in future field development.

The mercury injection capillary pressure (MICP) lap test was used by El Sayed et al. (2019) to characterize the pore throat radius and classify the hydraulic flow units of Bahariya reservoir into ten hydraulic flow units governed by lithology variations and flaser laminations as direct impact of sedimentation and diagentic processes.

The cation exchange capacity (CEC) was not considered in the study area before as one of the shaley sand key methods. The recent water saturation analysis of dean stark is used in validating models of minimum saturation error. Furthermore, the Elan models were applied before in similar fields but not in the study area where this model is used to fine-tune the net pay reservoir and to identify the matrix and cement contents.

**Geologic setting**

Abu Gharadig basin is one of the Western Desert large-scale structural provinces, (Meshear 1990; EGPC 1992; Schlumberger 1995; Dolson et al. 2001). During the late Cretaceous, axis of the Abu Gharadig basin was mainly trending east–west occasionally associated with northeast trend, these trends control the deposition in the basin and the structural deformation was controlled by the E–W to ENE oriented faults (Bayoumi 1996) (Fig. 2). The basin consists of several ENE elongated pull apart grabens formed in the early Cretaceous and most of Abu Gharadig faults die out on the Apollonia formation (Abdel Aal and Moustafa 1988; Bakry 1994, 2005; Bayoumi 1996; Ibrahim 2014).

The study area is located between the Kattania and Mubarak highs affected by a series of extensive compression known as the “Syrian Arc” trending northeast–southwest (Moustafa...
The Bahariya Formation is a sedimentary sequence deposited in a shallow marine to near-shore environment at the beginning of the Late Cretaceous (Cenomanian) transgression in the Western Desert of Egypt (Said 1962, 1990; El Ayouty 1990; Wahdan et al. 1996). Barrier bars, stream mouth bars, point bars and distributary channels are the identified facies in the Bahariya Formation (El Sayed et al. 1993) encountered in the Salam and Khalda oil fields.

The Bahariya reservoir is subdivided into two unit’s separated by laterally extended geo-markers (flooding shale or paleosoles). The middle and lower Bahariya reservoirs of late Cretaceous age are described as overall transgressive sequence with few stacking cycles (Mahsoub et al. 2012) (Fig. 3). The Lower/Middle Bahariya reservoirs are interpreted to be deposited in a shallow marine/marginal marine depositional environment (Franks 1982;
Catuneanu et al. 2006; Halisch et al. 2009; Bakr et al. 2010).

Data and methods

The present work is discussing shaley sand impact on water saturation for the hydrocarbon-bearing reservoirs in Neag-1 and Neag-2 oil fields. Bore hole logs are used to determine the petrophysical properties of the Bahariya shaley sand reservoirs using the Techlog software (Table 1). Core analysis is also used to calibrate the petrophysical parameters as porosity ($\phi$) and water saturation ($S_w$) which calculated from logs (Table 2). The water saturation is measured in laboratory using the distillation method of Dean and Stark (1920) and according to API recommended practice 1998. The distillation method is a direct method for measuring water saturation from a core plug, while the cation exchange capacity (CEC) is the indirect method utilized to calculate the shale effect on electrical resistivity. CEC is defined as the excess conductivity caused by the clay minerals. CEC is measured in lap to fully brine saturated plugs of variable salinities as per Waxman and Smits (1968), Juhasz (1981) and Crain’s Petrophysical Handbook (2000).

The calculated $S_w$ from Archie model is reaching 80% in some intervals, while the initial production data for these intervals indicated 0% water production. These production data challenged the saturation by Archie model for the Bahariya reservoir (El-Bagoury 2015, 2019).

Well log analysis

The objective of this process is to evaluate the Bahariya reservoirs using recorded bore hole logs to detect the net hydrocarbon-bearing zones and calculate the different petrophysical parameters (such as $V_{sh}$, $\phi_e$ and $S_w$). The presence of clay minerals is affecting the gamma ray and resistivity tool response, which may bias the definition of the true formation saturation only from bore hole logs. The formation evaluation workflow used in this study is schematically shown in Fig. 4.

Shale volume is calculated by gamma ray method using linear relationship (Schlumberger 1972, 1989). Porosity is calculated from porosity logs, density logs, neutron logs and sonic logs using Wyllie Equation 1950. Porosity from
Fig. 3 North Western Desert Stratigraphic column (WEC 1995 by Schlumberger)
density equations was discussed in Dresser Atlas (1979, 1983). The constants and parameters used in the well log analysis are tabulated in (Table 3).

Ten core samples were acquired for cation exchange capacity test in different intervals of the Bahariya reservoir. The different log readings against each CEC sample are tabulated in Table 4.

### Lithology and Mineralogy

Bahariya reservoir is of mixed lithology nature consisting of sand, shale and carbonates. Lithology can be identified from gamma ray, density, neutron and photoelectric logs which are widely available in the field wells. These four logs are easily used to classify the three Bahariya lithologies, but to differentiate the rich clay sandstone complex mineralogy more logs are required for proper resolve. The accurate mineral solve is requiring advanced logging tools which are not available in NEAG fields. It’s difficult for the non-operated wells and expensive to implement. The Bahariya formation consists of different minerals as illite, kaolinite, smectite, chlorite, k-feldspar, calcite, siderite, quartz and mica in variable amounts (Shokry et al. 2015).

The core reports and legacy of nearby fields showed the next percentages, quartz (50–60%), calcite and siderite (0–20%), kaolinite (5–15%) and shale matrix (10–20%) (Wehr et al. 2002; Shokry et al. 2015).

Siltstone is rich clay lithology of finer grain size comparing to sandstone and in order to differentiate from shaley sand and shale spectral gamma ray is fully utilized to differentiate between Bahariya reservoir clay minerals illite, kaolinite, smectite and chlorite. Sonic log is also used essential to differentiate between the carbonate minerals calcite and siderite. A Quanti-Elan model is computed by Techlog software. The calculations are a lengthy linear mathematics where the number of logs equal the number of unknown rock minerals, these hybrid algorithms done by the software. The input parameters for each mineral were set up after a set of iterations to characterize those mixed lithologies. The input parameters of this model are summarized in Table 5. The output minerals are calibrated with composite logs and petrography reports at different intervals to validate this Elan model but the full package of data is limited for the public domain.

| Table 1 | Summary of available well log data |
|---------|------------------------------------|
| Bore hole logs | Neag-1 | Neag-2 |
| Gamma ray | √ | √ |
| Spectral GR | √ | X |
| Photoelectric factor | √ | √ |
| Shallow resistivity ($R_s$) | √ | √ |
| Deep resistivity($R_d$) | √ | √ |
| Neutron ($\varnothing$) | √ | √ |
| Density ($\varrho_b$) | √ | √ |
| Bore hole image (BHI) | √ | √ |
| Compressional sonic ($V_p$) | √ | X |

| Table 2 | Summary of available core analysis data |
|---------|----------------------------------------|
| Analysis | Number of plugs | Neag-1 | Neag-2 |
| Cation exchange capacity, CEC | 10 | √ | X |
| Water saturation, Dean Stark | 5 | X | √ |

**Fig. 4** Well logs interpretation workflow

| Table 3 | Constants and parameters used in the well log analysis |
|---------|--------------------------------------------------------|
| $Gr_{min}$ | 35 API |
| $Gr_{max}$ | 120 API |
| $Gr_{int}$ | 2.69 g/cm³ |
| $Gr_{int}$ | 0.95 g/cm³ |
| $R_w$ | 0.035 Ohm m |
| $R_d$ | 0.6 |
| $\varrho_m$ | 2 Ohm m |
| $\Delta T_m$ | 52 $\mu$s/ft |
| $\Delta T_f$ | 189 $\mu$s/ft |
Electrofacies analysis

Thomas and Stieber (1975) method is used to identify the different types of shale by plotting volume of shale ($V_{sh}$) versus total porosity ($\phi_t$) (Fig. 5). Structure and dispersed shales are rarely found relative to the other types. Clean sand, laminated sand and siltstone are the three main categories observed in the Bahariya reservoir. The laminated shaley sand lithology is an intercalation of sand and shale layers on small scale commonly at or below the log resolution which will affect the log readings. These intercalations known as hetrolithics or sand flats are the key element to evaluate the Bahariya reservoir potential (El-Bagoury et al. 2017). The siltstone has finer grain size and higher degree of shaliness.

Shaley sand models

This work is done after characterizing the clay types in the Bahariya reservoir to review the calculated water saturation using the appropriate models. Calculated water saturation by shaley sand models is significantly decreased by 30% from water saturation by Archie which is matching with production data (dry oil). The next section will discuss these methods.

Indonesian model

The Indonesia equation by Poupon and Leveaux (1971) was developed for shaley sand reservoirs in fresh formation water with salinities less than 20,000 NaCl ppm. The water saturation is function of deep resistivity ($R_t$), while
the resistivity of shale ($R_{sh}$) is taken from resistivity logs against pure shale zones.

$$\frac{1}{R_t} = S_w^{n/2} \left[ \frac{V_{sh}}{R_{sh}} \sqrt{\frac{1}{n} - \left( \frac{V_{sh}}{R_{sh}} \right)^{n/2}} \right] + \left( \frac{\theta_e^{m/2}}{\sqrt{m} \cdot R_w} \right)$$

where $R_t$: true (deep) resistivity in the un-invaded zone (Ohm-m); $S_w$: un-invaded zone water saturation (fraction); $V_{sh}$: volume of shale (fraction); $R_{sh}$: resistivity of shale (Ohm-m); $\theta_e$: effective porosity (fraction); $m$: cementation factor; $a$: constant multiplier; $R_w$: formation water resistivity (Ohm-m).

**Simandoux model**

Simandoux studied the clay volumes effect on reducing rock matrix conductivity and the water saturation. Simandoux experiments on 1963 discussed clay effect on homogeneous mixtures of sorted sand and natural clay in various proportions which artificially mixed on laboratory.

$$S_w = \frac{a \cdot R_w \cdot (1 - V_{sh})}{2\theta_e^m} \left[ -\frac{V_{sh}}{R_{sh}} \right] + \left( \sqrt{\left( \frac{V_{sh}}{R_{sh}} \right)^2 + \left( \frac{4\theta_e^m}{a \cdot R_w \cdot R_t \cdot (1 - V_{sh})} \right)} \right)$$

where $S_w$: un-invaded zone water saturation (fraction); $V_{sh}$: volume of shale (fraction); $R_{sh}$: resistivity of shale (Ohm-m); $R_w$: Formation water resistivity (Ohm-m); $R_t$: true deep resistivity in the un-invaded zone (Ohm-m); $\theta_e$: effective porosity (fraction); $a$ and $m$ are constants representing multipliers and cementation factors, respectively.

**Waxman Smith model**

Waxman and Smits method based on the laboratory measurements for cation exchange capacity (CEC) versus shale content. CEC measured on core samples are correlated with effective porosity and shale content calculated from logs. Log-derived porosity and shale volume are usually necessary for accurate water saturation calculations.

The equation is as follows:
where $R_t$: true resistivity in the un-invaded zone (Ohm-m); $S_w$: the un-invaded zone water saturation (fraction); $R_w$: the formation water resistivity (Ohm-m); $F$: formation factor. $\frac{1}{\Omega_m}$ where $m* \neq m$; $Q_v$: cation exchange capacity volumetric (Unit per liter); $B$: Equivalent cationic conductance of a sodium ion (L S/m) can be calculated by next equation to relate $B$ to formation temperature ($T$) Celsius degrees and water resistivity, $R_w$, as published by Waxman and Thomas (1974), is as follows:

\[
\frac{1}{R_t} = \frac{S_w^2}{F} + \frac{BQ_v \ast R_w}{F}
\]

(3)

\[
B = \left( \frac{-1.28 + 0.255^*T - 0.0004059 \ast T^2}{1 + (0.04^*T - 0.27) \ast R_w^{1.23}} \right)
\]

(4)

Normalized Waxman–Smits equation ($F = 1/\Omega_m$), where $\Omega$ is derived from the density log and corrected for hydrocarbon effects. Water saturation is calculated in total interconnected pore spaces (Juhasz 1981). Estimating the apparent water conductivity according to the next equation:

\[
\frac{\Omega_m}{R_t} = BQ_v + \frac{1}{R_w}
\]

(5)

Fig. 6 Well-1 integrated plot for well logs, core analysis, core photographs, borehole Image and lithology modified from ElBelisy et al. (2010)
where $m^*: modified cementation factor; \Phi: formation porosity (fraction); R_T: true resistivity in the un-invaded zone (Ohm-m); BQ_v: Cation exchange capacity (Unite per liter); R_w: water resistivity (Ohm-m).

The cation exchange capacity is calculated by the equation:

$$BQ_v = BC \frac{(\theta_N - \theta_T)}{\theta_T}$$  \hspace{1cm} (6)

BC is the slope of this relation at 100% water saturation of the relation between apparent water conductivity $\left( \frac{\mu_w}{K_w} \right)$ versus apparent clay fraction conductivity $\left( \frac{\theta_C - \theta_T}{\theta_T} \right)$.

Low resistivity pay

Low resistivity pay module (also called LowReP) is considered to evaluate laminated sand/shale reservoirs. The application of this method into dry oil productive zones characterized by high clay content to correct the excess conductivity rise compared with rock (Darling 2005).

Low resistivity pay module workflow applied in steps as follows;

1. The input curves require at least GR, density, neutron and resistivity curves.
2. Estimating $V_{sh}$ from neutron/density logs.
3. Define the cutoff limit.
4. Calibrate with core measurements or test results (the simple calibration is the ultraviolet core photographs that affected by oil staining (Fig. 6).
5. The shale parameters estimated for low resistivity pay are as follows;

| Parameters          | Gamma ray API | Bulk density (g/cm³) | Neutron porosity |
|---------------------|---------------|----------------------|------------------|
| Shale parameters    | 110           | 2.45                 | 0.35             |

6. The anisotropy correction is the key factor in which this method was the apparent vertical resistivity corrected to remove the laminated clay effect, which found approximately equals 1.5 the horizontal resistivity.

$$\frac{R_v}{R_h} \cong 1.5$$  \hspace{1cm} (7)

Results

The scope of this work is to identify the petrophysical properties for Bahariya shaley sands specially water saturation ($S_w$) and compare the log evaluation results to core measurements for calibration. The degree of shaliness is classified into low, medium and high. The overall reservoir shows non-clean formation trend and different mineral composition. Various water saturation models are considered in petrophysical evaluation, and the average error between the log results and core data is highlighted.

Porosity calibration

The calculated water saturation is function of log porosity. The error in log porosity will affect the quality of water saturation calculation. Thus, the log porosity is calibrated with core porosity measured in laboratory. This calibration is applied to the results to check for minor errors. This step is providing quality assurance to results and linking between different petrophysical methods (Darling 2005; Schön 2011). The calibration is significant for porosity calculation in future wells from logs only in the non-cored wells. Log porosity and core porosity plotted against each other in two different plots

1. Log plot, the log porosity is plotted with same scale as red circles in the same track of log porosity for visual correlation (Fig. 7).
2. $X$, $Y$ plot, the log porosity is plotted on $X$ axis versus log porosity on $Y$ axis to quality control the best fit line (Fig. 8).

There is a strong match and harmony between the calculated log porosity and measured porosity form core samples up to 85% of the data.

Shaley sand count

The bore hole image (BHI) has a high vertical resolution (0.2 in. in water base mud and 0.4 in. in oil base mud) while the conventional logs are more than 8 in. (Schlumberger technology forum 2010). High-resolution bore hole image is used in net sand count to calibrate neutron/density cross-over and Thomas Stiber plot to fine-tune the shaley sand cutoff. Each electrofacies is calibrated by BHI using the separation between neutron and bulk density logs (Fig. 9). Each code represents different facies;

| Code 1 | Clean sand where clear cross over between the neutron and bulk density logs. |
| Code 2 | Shaley sand (sand flat) where the two logs are closer and no big gaps between. |
| Code 3 | Siltstone where the logs have narrow negative cross over. |
| Code 4 | Shale where the logs separation is clear negative crosses over. |
Elan model (with complete log data set) is used to differentiate between different pore filling minerals especially clay minerals (kaolinite, illite and k-feldspar) from other finer shales in rock matrix. The Elan model in this paper is targeting accurate net pay sand and digital mineral components against all intervals (Fig. 10). The output minerals curves of Bahariya reservoir showed total seven common minerals after the modeling process. These minerals are Illite, kaolinite, calcite, siderite, quartz (sand), shale and rare amount of k-feldspar while chlorite and smectite are absent. Few bad hole flags are highlighted in red color due to washout. There is high concentration of kaolinite in few intervals of lower Bahariya, which increases the recorded gamma ray and density logs (Fig. 10).

Discussion

The shaley sands are the common electrofacies in Bahariya reservoir if shale is ignored with up to 27% from total. Structure and dispersed shales are rare and does not exceed 3%. The careful inspection of shaley sands in the core photographs ultraviolet light showed oil staining as same as
the clean sands (Fig. 6). Thus, shaley sands can be added to the net pay reservoir and selected for further perforation. On the other hand, the siltstone electrofacies does not exceed 11% in total of Bahariya Formation. Generally, siltstone does not show positive oil staining on ultra-violet light like shaley sands as the storage capacity of siltstone is limited in these types of rocks (El Sayed et al. 2019). Therefore, the siltstone electrofacies is not considered as part of the net reservoir (Fig. 11).

Storage and flow capacities of Bahariya reservoirs are affected rigorously by amount of pore filling minerals especially calcareous cements (Shokry et al. 2015; El Sayed et al. 2019); the carbonate cements influence the CEC as well. Carbonate minerals (calcite and dolomite) are interrupting the correlation between volume of shale, porosity and cation exchange capacity (Figs. 12, 13).

The CEC can be expressed by the equation:

\[
\text{CEC}^* = -11.635 \left[ (1 - \phi^*) V_{sh} \right]^{3.49}
\]  

(8)

Core conductivity measurements give range of CEC from \(-0.07\) to \(-1.08\) S/m. Waxman smith cementation factor \((m^*)\) is ranging from 0.7 to 1.6. This method benefits from the three reservoir groups mentioned earlier (1) clean sand, (2) shaley sand (sand flat) and (3) siltstone. CEC is integrated with each type in Table 6.

Four methods were applied to calculate water saturation from bore hole logs. The comparison between these methods is proving a conclusion about the true water saturation. The calculated error in the water saturation by Indonesia is higher than other methods. Simandoux gives better water saturation results than Indonesia and LRp, which are showing uncertainty above and below the core measurements. Waxman smith showed calibrated results comparing with Dean stark saturation measured on core for the same intervals. Waxman smith and Simandoux methods enhance the water saturation to reasonable values matching the core measurements although there is still small error that does not exceed 9% of the true saturation mainly observed at very low porosity (Table 7). The advantage of integrating all these
| Depth | Gamma ray | Sonic Log | Spectral GR | Density Neutron | Bad hole Flag | Elemental Mineralogy |
|-------|------------|-----------|-------------|-----------------|---------------|---------------------|
|       |            |           |             |                 |               |                     |

**Fig. 10** Elan model input logs, output mineralogy, and interpreted lithology of pilot well

**Fig. 11** Bahariya histogram for types of shale

| Shale Types | Structural | Siltstone | Clean Sand | Shale | Shale Sand | Dispersed |
|-------------|------------|-----------|------------|-------|------------|-----------|
|             | 0.9        | 10.9      | 14.5       | 44.5  | 27.5       | 1.8       |
| Distribution | 0.9        | 10.9      | 14.5       | 44.5  | 27.5       | 1.8       |
| Cumulative Frequency | 0.9 | 11.7 | 26.2 | 70.7 | 98.2 | 100.0 |

**Fig. 12** CEC versus volume of shale in Bahariya reservoir

**Fig. 13** CEC versus porosity of Bahariya reservoir
Table 6  Cation exchange capacity integrated characterization

| Shale type     | CEC (S m⁻¹) | V_shale (%) | V_silt (%) | V_sand (%) |
|----------------|-------------|-------------|------------|------------|
| Clean sand     | 0 to –0.1   | < 25        | 5–10       | 70         |
| Shaley sand    | –0.15 to –0.5 | 30–40   | 10–20      | 60         |
| Siltstone      | –0.5 to –0.9 | > 50       | 20–30      | < 50       |

Table 7  Integrated water saturation results of core and log interpretation on same plugs

|          | Porosity (%) | Dean stark (%) | Indonesia (%) | Simandoux (%) | Waxman Smith (%) | Low resistivity pay (%) |
|----------|--------------|---------------|---------------|---------------|------------------|------------------------|
| Sample-A | 18.8         | 18.1          | 25.5          | 20.0          | 12.94            | 22.22                  |
| Sample-B | 11.1         | 20.1          | 30.0          | 21.75         | 16.81            | 35.71                  |
| Sample-C | 21.4         | 13.6          | 33.0          | 22.0          | 20.73            | 6.67                   |
| Sample-D | 6.2          | 26.3          | 35.0          | 25.0          | 35.23            | 8.11                   |
| Sample-E | 16.3         | 20.7          | 30.7          | 23.76         | 15.53            | 17.86                  |
| Average error | 0      | 11.08        | 2.74          | 0.49          | –1.65            |                        |

Fig. 14  Well-1 litho-saturation cross-plot of the Bahariya reservoir in NEAG-1
methods will be clear in water-bearing reservoir intervals, as no pseudo-hydrocarbon saturation will appear (Figs. 14, 15).

The results showed variation in water saturation. Simandoux provides a reasonable correlation with saturation in core; however, this method is only log-derived regardless the shale distribution. Simandoux method looks uniform in all Bahariya shale types without unique clay mineral characterization as Waxman smith method. The Waxman smith error is very small due to the effective calibration with CEC measurements. The low resistivity pay method gives an optimistic correction to clay content based on the percentage of shale intercalations identified from bore hole images which give the applied vertical correction assuming homogeneous layers and unique clay resistivity response. The LRp method is mainly based on that assumption; however, it may not be the case for the Bahariya reservoir. The average water saturation for each tested method is found in Table 8.

**Conclusions**

The derived water saturation by different petrophysical models from bore hole logs is compared to core measurements in the same intervals. Three types of electrofacies are detected in Bahariya reservoir rocks subjected to clay percentage, clean sandstone, shaley sandstones and siltstones. The high-resolution bore hole image and Quanti-Elan model are used to validate and calibrate the three electrofacies. Shaley sand of the Bahariya reservoir is rich in kaolinite, illite and carbonate cement, which increases the matrix density up to 2.69 g/cc. Clean and shaley sand electrofacies are considered the best reservoir with average porosity 26% and 21.5%, respectively, while siltstone is considered as poor

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**Table 8** Results of different saturation methods

| Method               | Indonesia | Simandoux | Waxman Smith | Low resistivity pay |
|----------------------|-----------|-----------|--------------|---------------------|
| Average water saturation (%) | 30.84     | 22.50     | 20.25        | 18.11               |

**Fig. 15** Well-2 litho-saturation cross-plot of the Bahariya reservoir in NEAG-2
reservoir characterized by average porosity 17.6% and high clay content (35–55%). The upper part of Bahariya reservoir showed differences in porosity because of variation in grain size and clay contents as result of fining and coarsening upward associated with cemented layers sometimes. The interpreted electrofacies are integrated with CEC to apply Waxman smith method. The clean sand reveals neglected CEC while shaley sands have CEC ranging from −0.15 to −0.5 S/m and siltstone from −0.5 to −0.9 S/m. The empirically calculated CEC from volume of shale and porosity gives coefficient of correlation higher than 0.9 which can be extended to other fields. Waxman smith approach gives minimum error which is considered the best method for calculating water saturation in Bahariya shaley sands followed by Simandoux in second place. Simandoux method showed relatively small error (2–3%) comparing to Waxman smith. Generally, Simandoux method gives good estimations and LRp gives low Sw results.

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