INTRODUCTION

The effects of anthropogenic or natural pressures applied to any part of an ecosystem are eventually felt everywhere to some extent through the phenomenon known as a ‘trophic cascade’ (Pace et al., 1999). Cascading effects are attenuated or amplified as they propagate through the food web, depending on the nature of the pressure and details of the ecology (Heath et al., 2014). Diagnosing the type and magnitude of pressures that an ecosystem can sustain before being fundamentally altered requires simulation with mathematical models that aim to represent the key ecological components and processes which govern cascades.

We present the package STRATH-E2E2 for the R statistical environment (R Development Core Team, 2014), which models both bottom-up and top-down trophic cascades in shelf-sea ecosystems, spanning inorganic and organic nutrients through to birds and mammals. The model takes a macroscopic view of ecology, aggregating over the many microscopic details of taxonomy, demography and spatial structure (Giricheva, 2015). The aim is to represent the gross dynamics with a tolerable parameter count and fast run-time, so as
to enable ‘big-picture’ strategic scenario analyses. The basic model is supported by functions for computational parameter optimization, sensitivity analysis, estimation of credible intervals of model outputs and network analysis.

2 | MODEL DESCRIPTION

2.1 | Ecology model general description

The ecology model, developed from an earlier prototype (Heath, 2012), is a network of mass conserving coupled ordinary differential equations (ODEs) describing spatially averaged rates of change in state variables representing organic detritus, dissolved inorganic nutrient and living biomass. To simplify the description we can think of the variables as being divided between two coupled sub-networks: a predator-prey network—the food web—and a nutrient recycling network. Between the two, all marine life-forms are explicitly or implicitly accounted for, but aggregated into coarse groups or ‘guilds’ defined mainly by feeding characteristics and diet preferences (Figure 1). All state variables, except macrophytes, are expressed solely in terms of nitrogen mass, since this element is the most commonly limiting in temperate shelf seas. Macrophytes are expressed in terms of both nitrogen and carbon mass with dynamic stoichiometry since these organisms have an exceptional capacity to seasonally absorb and store nitrogen (Appendix S1).

Each ODE comprises a set of rate-of-change terms representing a variety of biological and physical processes (Appendix S1). Biological terms describe the balance between gains due to assimilation of food, and losses due to mortality and metabolism. Some components of the food web (planktivorous and demersal fish; suspension/deposit feeding and carnivore/scavenger feeding benthos) are resolved into life stages, and for these the equations...
also include the balance between gains due to recruitment and losses due to developmental progression or spawning. In addition, all components of the model are replicated across homogeneous spatial compartments, so each ODE also includes terms representing sinking, advection, mixing and migration flows through the system.

The model has a coarse spatial structure consistent with the coarse guild definitions of the living and chemical components of the system. The spatial domain is first divided horizontally into two bathymetric/hydrographic zones (Figure 2) which represent the most basic spatial division in shelf seas—a shallow, vertically mixed zone mostly influenced by tides and freshwater inputs, and a deeper, potentially seasonally stratified zone mostly influenced by exchange with an external ocean (Pingree & Griffiths, 1977).

For convenience we refer to these as the inshore and offshore zones respectively, though there is no necessity for the inshore zone to be adjacent to the coast—in principle it could represent a shallow offshore bank. The water column in the offshore zone is divided vertically into two compartments or layers, while the inshore zone is represented by a single compartment. The inshore and offshore zones are each divided into discrete seabed habitat types comprising exposed rock and up to three compartments of different sediment properties per zone. The sediment habitats are notionally mud, sand and gravel, but defined by median grain size and natural disturbance rates. It is not necessary or computationally efficient to represent each state variable in every spatial compartment; for example, cetaceans do not need to be resolved vertically. State variables are therefore resolved hierarchically to spatial compartments with the largest (in terms of body size) and/or most mobile guilds being represented at the coarsest spatial resolution (Appendix S1).

2.2 Predator–prey connections, demography and mortality

Ingestion of prey by a predator is governed by a preference matrix and a standard Type II functional response in which per-unit-biomass predator consumption rates increase asymptotically towards a $Q_{10}$ temperature-dependent maximum with increasing prey concentration (Appendix S1). A proportion of ingested food becomes new body mass in the predator. The remainder is divided equally between fluxes to organic detritus and ammonia, to represent defecation of undigested material and food-dependent metabolism. Background (non-feeding) metabolism increases with temperature but with a higher $Q_{10}$ than maximum uptake rates, so the net result is that productivity, that is, production rate per unit biomass, will exhibit a dome-shaped response to temperature.

2.3 Nutrient recycling network

Six forms of organic detritus are represented in the recycling network: suspended material, labile and refractory sediment material, ‘macrophyte debris’, ‘corpses’ and ‘discards’. Both the suspended and sediment fractions implicitly include dissolved and particulate organic matter and associated bacterial flora, and are formed in the living food web by defecation and density-dependent mortality fluxes from plankton and the larval stages of fish and benthos. Corpses are produced by density-dependent mortality of fish, benthos and top predators, and the decay of discards. The latter are a short-lived, special form of detritus generated as a by-product of fishery harvesting. Macrophyte debris is created by wave and density-dependent destruction of living macrophyte forest biomass. All forms of detritus are regarded as a potential food source for detritivorous and scavenge feeding guilds of living organisms.

The dynamics of each detritus and dissolved nutrient category are governed by an ODE in which the rate-of-change terms correspond to the production and consumption rates elsewhere in the food web, plus physical flows between spatial compartments. $Q_{10}$ temperature-dependent coefficients govern transformations between different forms of detritus, conversions of detritus into ammonia (mineralization); ammonia to nitrate (nitrification), and nitrate to nitrogen gas (denitrification). To complete the biogeochemical cycle, nitrate and ammonia are re-absorbed into the food web by phytoplankton and macrophytes, governed by light and temperature-dependent uptake responses.
2.4 | External boundary fluxes

Passive hydrodynamic influxes of dissolved nutrient, suspended detritus and phytoplankton into the model domain from adjacent sea areas are defined by driving datasets (Appendix S1). These comprise water volume influxes and associated boundary concentrations of advected material, the products of which (volume flux × concentration) represent mass fluxes. These are incorporated into the rate terms in the relevant ODEs describing changes in the receiving spatial compartments (Appendix S1). Additional inflows due to dry and wet deposition of atmospheric nutrient to the sea surface, nutrient inputs from river discharges, and other unspecified sources (e.g. aquaculture) are accounted for in the same way.

The proportions of dissolved nutrient, suspended detritus and phytoplankton passively exported from the model domain are calculated dynamically assuming conservation of fluid volume, that is, data-driven volume inflows to each compartment are matched by calculated outflow volumes, with the associated mass transport dependent on compartmental concentrations. Other passive exports from the domain are losses of gaseous nitrogen generated by denitrification, burial of refractory organic nitrogen in the sediments, beach-cast of macrophyte debris, and extraction of biomass by fishing.

The model also provides for active immigration and emigration of a migratory fish guild across the external boundary. Examples of such taxa would be tuna or mackerel which undertake ocean-scale migrations, transiting through regional ecosystems en-route. The ocean stock is treated as a fixed boundary condition and the proportion entering the model domain each year parameterized from, for example, survey data. Emigration is defined by a time varying proportional loss rate from the guild to an ocean sink.

2.5 | Interior fluxes between spatial compartments

The vertical and horizontal links between sediment and water column compartments within the model domain are represented by combinations of passive advection, diffusion and sinking and active migration fluxes (Appendix S1). Dissolved nutrients, detritus and phytoplankton are subject to passive vertical and horizontal exchanges. Zooplankton and larvae of fish and benthos are subject to passive horizontal exchanges, but active vertical. Fish and top predators (pinnipeds, cetaceans and birds) undertake active horizontal migrations, but their vertical distributions are not resolved.

Passive exchanges are the product of dynamic differences in concentrations between vertical or horizontal spatial compartments, scaled by hydrodynamic mixing coefficients supplied as time-varying parameters (Appendix S1). Mixing coefficients between sediment habitats and the water column are defined by sediment permeability, modified by representations of bioturbation by deposit feeding benthos, natural erosion by bed shear stress and fishing-related abrasion.

In reality, plankton and larvae undertake active diel vertical migrations but we do not resolve these sub-daily behaviours. Rather, we aim to represent the daily average vertical distributions of their prey ingestion, excretion and defecation. Hence, the proportional vertical distributions of these fluxes are distributed according to the preference-weighted vertical distributions of their detritus (microbial) and phytoplankton prey.

Active horizontal migrations are modelled explicitly. The mass fluxes between horizontal compartments are parameterized from the dynamic gradient in preference-weighted prey to predator ratios. Our aim is to reflect the body of research which shows that animals are simultaneously monitoring gradients in predators and competitors, as well as gradients in their prey when making migration decisions (Drackeley et al., 2015; Grant et al., 2014; Lamb et al., 2017).

2.6 | Representation of fishing in the ecology model

Living biomass guilds considered vulnerable to targeted capture or incidental by-catch by fishing gears are the top-predators (birds, pinnipeds and cetaceans); planktivorous, demersal and migratory fish; carnivorous/scavenge and suspension/deposit feeding benthos, carnivorous zooplankton and macrophytes. In each case, the fishing process is represented in the ODE for each guild by a ‘harvest ratio’ (proportion of instantaneous biomass captured per unit time). A proportion of the catch is directed to the discards class, comprising whole-animal rejects and viscera arising from at-sea processing of the remaining catch. Only the residual fraction of the catch weight is exported from the model as landings.

The collateral effects of fishing activity—release of sediment pore-water nutrients, resuspension of sediment detritus and damage mortality of benthos—are driven by the area-proportion of each seabed sediment habitat abraded per unit time by fishing gears.

2.7 | Fishing fleet model description

The fishing fleet model is a static, matrix-based scheme which generates harvest ratios and discarding rates for each guild in the ecology model, and abrasion rates for each seabed habitat, due to the combined actions of up to 12 different fishing gears. (Appendix S2). Key inputs are, for each gear type, the spatial distribution of activity density, catching power, selectivity, discards and at-sea processing rates for each ecology model guild, and contact rate with the seabed (Appendix S2). Activity density is defined as the deployment duration of a given gear per unit sea surface area in a given time interval, integrated across all vessels (units: m^-2). The power of a gear is a measure of its efficiency at catching biomass of a given resource guild. The product of activity density and power is a quantity that we refer to as fishing effort. For a given resource guild, effort is proportional to the harvest ratio and so can be summed across gears.
### 3 IMPLEMENTATION AND USAGE

**StrathE2E2** is provided as a package for the R statistical programming environment (R Development Core Team, 2014). This article describes version 3.2.0 for use with R version 3.6 or higher. The package is available for direct installation through R from CRAN (https://CRAN.R-project.org/package=StrathE2E2), while documentation and development versions are available from the GitLab site https://marineresourcemodelling.gitlab.io/index.html.

The core network of differential equations is coded in C for solving with the Isoda function as implemented in the 'deSolve' package for R (Soetaert et al., 2010). Isoda switches automatically between stiff and non-stiff methods—stiff methods are required when high rates of change are encountered to avoid numerical instabilities. All other operations are coded in native R, relying on only one other additional package (‘NETINDICES’, for computing network indices; Soetaert & Kones, 2014). The code is version controlled, and tested with a suite of scripts for the R ‘TESTthat’ package, currently with coverage of 92.8% (estimated with the package ‘COV’).

After loading the package into an R-session, type help(StrathE2E2) for an overview, including links to a User Manual, Cheatsheet (Appendix S5) and detailed documentation. All StrathE2E2 functions have cross-referenced html help files with examples of usage. These are accessible by typing help(function_name), or by following links from the package overview page.

All the model parameters and driving data inputs to the model are held in comma-separated ascii text (.csv) format. Model outputs are saved in R list-object structures, and also optionally mirrored to .csv files. The package includes an embedded model of the North Sea, with two versions representing different time periods (1970–1999 and 2003–2013). These may be copied to the user workspace and used as a template for development of new models.

Basic use of the model is illustrated here with an example based on the 2003–2013 version of the North Sea model:

```r
library(StrathE2E2) # Load the package
model <- e2e_read("North_Sea", "2003-2013") # Read inputs
```

Additional arguments of the e2e_read() function point to alternative models in the user’s workspace and manage output paths. The R object model is a list containing driving data and parameters loaded from .csv files specified by a configuration file MODEL_SETUP.csv located in the specified model workspace. Users have two avenues for developing scenario configurations involving, for example, changes in environmental drivers or fishing patterns—through coding to modify the model R object prior to executing a run (see User Manual and Data S1 for examples), or by editing the .csv input files.

```r
results <- e2e_run(model, nyears=5) # Run for 5 years
```

Running the model takes around 2 s per simulation year depending in hardware. The object results is a list containing all of the raw daily resolution model output and a suite of processed data products (annual averages of state variables, annual integrals of all fluxes, imports and exports including fishery landings, and a suite of annual network indices, for example, ascendency, redundancy).

Other functions offer a wide range of analysis and plotting options for model results. For example, the following function plots a time series of the daily values of ecological state ecological variables aggregated over the whole model domain for the full duration of a run:

```r
e2e_plot_ts(model,results) # Time series of output
```

Further functions are provided to undertake computational parameter optimization relative to a database of ecosystem observations, global sensitivity analysis (Morris, 1991; Wu et al., 2013), Monte Carlo simulations to generate credible intervals for model outputs (Appendix S3) and more. North Sea model example outputs from these computationally intensive functions are provided in a supplementary data package (StrathE2E2 examples). This automatically installs from the GitLab site when example data are first invoked from a relevant function, and remains silently present thereafter.

The package documentation includes guidance on how R users can extract data from the returned structures so as to conduct their own analyses. In addition, the .csv outputs offer language-neutral analysis options.

### 4 EXAMPLE MODEL OF THE NORTH SEA

The geographic domain for the North Sea example model provided with the package is divided between inshore and offshore zones at around the 30-m isobath (Appendix S4). The model was optimized for two contrasting periods of fishing, temperature, hydrodynamics and river nutrient emissions (1970–1999, cool temperatures and high harvest ratios for finfish; 2003–2013 warmer temperatures and low finfish harvest ratios), with a common set of biological parameters for the ecology model (Figure 3). Full details of the physical configuration, assembly of driving data and the observational data for fitting are provided in Appendix S4.

As an example of the many possible ways of using the model to explore scenario situations, Figure 4 shows the difference between a baseline model representing the stationary state with 1970–1999 environment and fishing activity, and the stationary state for a scenario in which all towed fishing gears are prohibited in the inshore zone and displaced offshore. Note that the overall activity rates of the gears remain unchanged. This scenario directly affects the fish and benthos guilds which are the main targets of the mobile fishing gears. However, the ecosystem response also extends to cetaceans, pinnipeds, birds,
zoooplankton, phytoplankton and nutrients through indirect ‘who-eats-whom’ network effects which cascade through the food web. Other illustrative scenario experiments are presented in Appendix S4.

5 | APPLYING THE MODEL TO NEW REGIONS

The ease of applying STRATH-E2E2 to a new region will depend on the availability of driving data, and observational data to form...
the target for parameter optimization and sensitivity analysis. Development, assembly and refining of these data for the North Sea model was a substantial task, but copying and adapting this setup to represent a different region is well within the scope of, for example, a Masters or PhD project. Our experience is that a credible draft model can be produced in a few days by roughly adapting the North Sea example given basic knowledge of the environmental driving conditions such as annual cycles of light and temperature, bathymetry, seabed sediment properties and fishing fleet compositions.

6 | DISCUSSION AND FUTURE DIRECTIONS

There is no simple answer to the question of an appropriate spatial, taxonomic and biological granularity for an ecosystem/food web model (Fulton, 2010; Giricheva, 2015; Iwasa et al., 1987). In STRATH2E2, our aim was to provide a ‘big picture’ marine ecosystem modelling tool amenable to computational parameter optimization, sensitivity analysis and exploration of uncertainty in model outputs, on ordinary desktop computing hardware. Achieving this required us to sacrifice some spatial, taxonomic and biological granularity in order to span the ecosystem and food web from physics, nutrients and microbes through to megafauna and fishing fleets. Other end-to-end models which aim to represent the system at greater granularity (e.g. Atlantis; Audzijonyte et al., 2019) pose substantially greater implementation and computational challenges which impede comprehensive analysis of uncertainty. Partial models, which dynamically represent only a subset of taxa of interest at greater spatial, taxonomic or demographic resolution (e.g. Ecopath with Ecosim (which does not dynamically represent the physics, nutrient or microbial system, Christensen & Walters, 2004); Speirs et al., 2010; Scott et al., 2014) can be problematic for simulating cascading effects because propagation is sensitive to the way in which boundary conditions are represented, especially for short food chains (Heath et al., 2014).

Inclusion of tools for exploring uncertainty in model outputs and parameter sensitivity is a relatively new development for ecological modelling packages (Steenbeek et al., 2018; Wu et al., 2013). However, interfaces to these techniques are among the essential requirements for future generations of models, allowing uncertainty in the outputs to be attributed to different sources of uncertainty in the inputs (Pianosi et al., 2016). This is increasingly required for corroboration, quality assurance and the defensibility of model-based scenario analyses. In the STRATH2E2 package, we have provided integrated analysis functions based on some established methods (Simulated Annealing for optimization, Morris Method for sensitivity analysis), but there are many other methods available (e.g. Sobol Methods; Sobol, 2001), and Bayesian methods using Markov chain Monte Carlo algorithms). Users can explore these by simply embedding our e2e_run() function (which executes a single model run with a given parameter set) into their own scripts to encode different methodologies.

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AUTHORS’ CONTRIBUTIONS

M.R.H. conceived and led the project, developed the original code and the North Sea implementation, and wrote the paper and supporting materials; D.C.S. co-supervised staff involved in the supporting material and contributed to the model design; I.T. converted the research code into an operational R package, developed the testing scheme and managed the GitLab site; R.J.W. contributed to the fishing fleet model and assembled the physical and fishery driving data for the North Sea implementation. All authors contributed to the drafts and gave final approval for publication.

PEER REVIEW

The peer review history for this article is available at https://publons.com/publon/10.1111/2041-210X.13510.

DATA AVAILABILITY STATEMENT

The package, complete with documentation, the North Sea model and all data shown in this paper, is available to download from CRAN (https://CRAN.R-project.org/package=Strath2E2) or the GitLab repository https://marineneresourcemodelling.gitlab.io/index.html.

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**SUPPORTING INFORMATION**

Additional supporting information may be found online in the Supporting Information section.

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