The discovery of high-energy (TeV-PeV) neutrinos from gamma-ray bursts (GRBs) would shed light on their intrinsic microphysics by confirming hadronic acceleration in the relativistic jet; possibly revealing an acceleration mechanism for the highest energy cosmic rays. We describe an analysis featuring three models based upon confronting the fireball phenomenology with ground-based and satellite observations of GRB030329, which triggered the High Energy Transient Explorer (HETE-II). Contrary to previous diffuse searches, the expected discrete muon neutrino energy spectra for models 1 and 2, based upon an isotropic and beamed emission geometry, respectively, are directly derived from the fireball description of the prompt $\gamma$-ray photon energy spectrum, whose spectral fit parameters are characterized by the Band function, and the spectroscopically observed redshift, based upon the associated optical transient (OT) afterglow. For comparison, we also consider a model (3) based upon averaged burst parameters and isotropic emission. Strict spatial and temporal constraints (based upon electromagnetic observations), in conjunction with a single, robust selection criterion (optimized for discovery) have been leveraged to realize a nearly background-free search, with nominal signal loss, using archived data from the Antarctic Muon and Neutrino Detector Array (AMANDA-II). Our preliminary results are consistent with a null signal detection, with a peak muonneutrino effective area of $\sim 80$ m$^2$ at $\sim 2$ PeV and a flux upper limit of $\sim 0.150$ GeV/cm$^2$/s for model 1. Predictions for IceCube, AMANDA's kilometer scale successor, are compared with those found in the literature. Implications for correlative searches are discussed.

1. Introduction

Neutrino astronomy may provide us with a new glimpse at the internal processes of gamma-ray bursts (GRBs). The Antarctic Muon and Neutrino Detector Array (AMANDA), which has been calibrated upon atmospheric neutrinos, has demonstrated the viability of high energy neutrino astronomy by using the ice at the geographic South Pole as a Cherenkov medium. Canonical fireball phenomenology \cite{1}, in the context of hadronic acceleration, predicts correlated MeV-EeV neutrinos from GRBs via various hadronic interactions \cite{2}. Ideal for detection are TeV-PeV neutrinos in coincidence with prompt $\gamma$-ray emission, resulting in a nearly background-free search. A detailed description of the modeling techniques and an ongoing analysis featuring correlated neutrino searches of individual GRBs from the Burst and Transient Source Experiment (BATSE) are described elsewhere \cite{3,2}. Here, we report on a complementary search for correlated leptonic ($\nu_\mu, \bar{\nu}_\mu$) emission, using models based upon the unique discrete electromagnetic characteristics and emission geometry of GRB030329, gleaned directly from satellite and ground-based observations. This represents a novel departure from searches \cite{4,5,6} based upon a diffuse formulation \cite{7}, which utilize averaged burst parameters.

2. GRB030329: Electromagnetic Emission & The GRB-Neutrino Connection

On March 29, 2003, at 11h37m14.67s (UTC), HETE-II was triggered by GRB030329 (H2652), a watershed transient which confirmed the connection between a core collapse Type Ic supernova and long duration GRB.
Electromagnetic investigations of the prompt $\gamma$-ray and multi-wavelength afterglow emissions associated with GRB030329 abound in the literature (see table 1), making it a perfect specimen for study. Via forward folding deconvolution, the photon energy spectrum was fit to the Band function \cite{8}, an empirically derived power law with smooth transition. For spectral indices $\alpha > -2$ and $\beta < -2$, the characteristic peak energy is defined as $E_p = [(2 + \alpha)E_{\gamma}^e(\alpha - 1)^{-1}]$, where $E_{\gamma}^e$ is known as the photon break energy \cite{8}. Hence, using standard error propagation, we find that $E_{\gamma}^e = 115.6 \pm 9.9$ keV. Doppler spectroscopy of the OT afterglow revealed a redshift measurement, which, under an assumed $\Lambda$CDM cosmology,\footnote{$\Lambda$CDM cosmology: $H_0 = 72 \pm 5$ km/Mpc/s, $\Omega_m = 0.29 \pm 0.07$, $\Omega_\Lambda = 0.73 \pm 0.07$ [Spergel et al., ApJS 148, 175-194 (2003)].} placed GRB030329 at a luminosity distance of $2.44 \pm 0.20 \times 10^{27}$ cm. Coupled with the peak energy flux, this implies an intrinsic peak isotropic luminosity of $L_{\gamma, iso} \approx 5.24 \pm 0.86 \times 10^{50}$ ergs/s in the 30-400 keV energy band pass. Evidence for anisotropic emission, in the form of a two component break in the afterglow spectrum, was revealed by radio calorimetry and is consistent with collimated prompt emission within a jet of opening half angle $\theta_{jet}$. This requires a beaming fraction correction, which reduces the intrinsic peak luminosity to $L_{\gamma, jet} = L_{\gamma, iso} (1 - \cos \theta_{jet}) \approx 1.99 \pm 0.33 \times 10^{48}$ ergs/s. Extended calorimetry provided an estimate for the fractions of shock energy imparted to the electrons ($\epsilon_e$) and magnetic field ($\epsilon_B$). Table 1 summarizes the observed electromagnetic properties used in this analysis.

The generic mechanism responsible for the super-Eddington luminosities associated with GRBs is the dissipation, via shocks, of highly relativistic kinetic energy, acquired by electrons and positrons Fermi accelerated in an optically thick, relativistically expanding plasma, commonly referred to as a fireball. The acceleration of electrons in the intense magnetic field of the fireball leads to the emission of prompt non-thermal $\gamma$-rays via synchrotron radiation. The temporal variability ($t_v \sim 10$ ms) in the light curves imply compact sources. In order to ensure a transparent optical depth to photons of energy $\epsilon_{\gamma, max} \approx 100$ MeV, a minimum bulk Lorentz boost factor ($\Gamma$) was assigned (see equation 20). Hadronic acceleration within the ambient photon field produces TeV-PeV leptons, via the following photosmeson interaction:

$$p + \gamma \rightarrow \Delta^+ \rightarrow \pi^+ + [n] \rightarrow \mu^+ + \nu_\mu \rightarrow e^+ + \bar{\nu}_e + \nu_\mu$$

(1)

Hence, these neutrinos are expected to be spatially and temporally correlated with prompt $\gamma$-ray emission. The

Table 1. Electromagnetic Properties of GRB030329: Prompt $\gamma$-ray and Multi-wavelength Afterglow Emission

| Parameter(s)                              | Value(s)                                      | Reference                    |
|-------------------------------------------|-----------------------------------------------|------------------------------|
| Positional Localization ($\gamma_{2000}$, $\delta_{2000}$, $\sigma_R$) | 16:1-2081646$^\circ$, 21.5215106$^\circ$, 3.0 \times 10^{-7}$ $^\circ$ | Taylor et al., GCN Report 2129 |
| Trigger (T) & Duration (T$_{500}$) [30-400 keV] | 41, 834.67 SOD, 22.8 $\pm$ 0.5 s | Vanderspek et al., ApJ 617: 1251-1257 (2004) |
| Energy Fluence ($F_{\gamma}$) [2-400 keV] | 1.630$^{+0.011}_{-0.013}$ $\times 10^{-4}$ ergs/cm$^2$ | Sakamoto et al., astro-ph/0409128 |
| Band Parameters ($\alpha$, $\beta$, $E_p$) [2-400 keV] | $-1.32 \pm 0.02, -2.44 \pm 0.08, 70.2 \pm 2.3$ | Vanderspek et al., ApJ 617: 1251-1257 (2004) |
| Peak Energy Flux ($\Phi_{\gamma, pk}$) [30-400 keV] | $\sim 7 \times 10^{-6}$ ergs/cm$^2$/s | Vanderspek et al., GCN Report 1997 |
| Spectroscopic Redshift ($z$) | 0.168541 $\pm$ 0.000004 | Bloom et al., GCN Report 2212 |
| Jet Opening Half Angle ($\theta_{jet}$) | $\sim 5^\circ \approx 0.09$ rad | Berger et al., Nature 426, 154-157 (2003) |
| Electron & Magnetic Field Energy Fractions | $\epsilon_e \approx 0.19$, $\epsilon_B \approx 0.042$ | Frail et al., ApJ 619, 994-998 (2005) |
parameterization of the neutrino energy spectra \( dN_{\nu_\mu}/d\epsilon_{\nu_\mu} \equiv \Phi_{\nu_\mu} \) traces the prompt photon energy spectra, as illustrated in figure 1 and is defined as follows [3, 9]:

\[
\epsilon_{\nu_\mu}^2 \Phi_{\nu_\mu} \approx A_{\nu_\mu} \times \begin{cases} 
\left( \frac{\epsilon_{\nu_\mu}}{\epsilon_{\nu_\mu}^b} \right)^{-\beta - 1} & \epsilon_{\nu_\mu} < \epsilon_{\nu_\mu}^b \\
\left( \frac{\epsilon_{\nu_\mu}}{\epsilon_{\nu_\mu}^b} \right)^{-\alpha - 1} & \epsilon_{\nu_\mu} < \epsilon_{\nu_\mu}^b \\
\left( \frac{\epsilon_{\nu_\mu}}{\epsilon_{\nu_\mu}^b} \right)^{-1} \left( \frac{\epsilon_{\nu_\mu}}{\epsilon_{\nu}^b} \right)^{-2} & \epsilon_{\nu_\mu} > \epsilon_{\nu_\mu}^b
\end{cases}
\] (2a)

\[
A_{\nu_\mu} \approx \frac{F_{\gamma} f_\pi}{8 \epsilon_{\nu} \ln(10) T_90} \approx 9.86 \times 10^{-4} \text{ GeV/cm}^2/s
\] (2b)

\[
f_\pi \approx 0.2 \times \frac{L_{\gamma,52}}{\Gamma_{2.5}^4 t_{v,-2} e_{\gamma,MeV}^b (1 + z)} \approx 0.77
\] (2c)

\[
\Gamma > 276 \left[ L_{\gamma,52} t_{v,-2} \epsilon_{\gamma,MeV}^{max} (1 + z) \right]^\frac{1}{b} \approx 178
\] (2d)

\[
\epsilon_{\nu}^b \approx \left[ \frac{7 \times 10^5}{(1 + z)^2} \right] \frac{\Gamma_{2.5}^2}{e_{\gamma,MeV}^b} \text{ GeV} \approx 1.404951 \times 10^6 \text{ GeV}
\] (2e)

\[
\epsilon_{\pi}^b \approx \left[ \frac{10^8}{(1 + z)^2} \epsilon_B \frac{1}{2} (L_{\gamma,52})^{-\frac{1}{2}} \Gamma_{2.5}^4 t_{v,-2} \right] \text{ GeV} \approx 7.9832941 \times 10^7 \text{ GeV}
\] (2f)

The values in equations (2b, 2f) are given for model 1, where \( L_{\gamma} \equiv L_{\gamma,52} \cdot 10^{52} \text{ ergs/s} \), \( \Gamma \equiv \Gamma_{2.5} \cdot 10^{2.5} \), \( t_v \equiv t_{v,-2} \cdot 10 \text{ ms} \), \( e_{\gamma}^b \equiv e_{\gamma,MeV}^b \cdot 1 \text{ MeV} \), and \( \epsilon_{\gamma} \equiv \epsilon_{\gamma,MeV}^{max} \cdot 100 \text{ MeV} \). Note the explicit dependence on discrete \( \gamma \)-ray photon observables.

3. Neutrino Astronomy with AMANDA-II: Analysis, Results & Discussion

AMANDA-II is comprised of 677 optical modules buried at depths between 1500-2000 m. The background consists of cosmic ray induced down-going atmospheric muons, detected at a rate of \( \sim 100 \text{ Hz} \), with a perturbation of atmospheric neutrinos, detected at a rate of \( \sim 10^{-4} \text{ Hz} \). The astrophysical neutrino signal, detected via charged current interactions such as: \( \nu_{\mu} + N \rightarrow \mu^+ + X \), is isolated by utilizing topologically identified up-going muon events, which are reconstructed by a maximum likelihood method. On-source, off-time data were used to estimate the stability of the background rate in order to maintain blindness, facilitating an unbiased analysis. After data filtering (see [10]), the total off-time background, excluding a 10 minute blinded window centered upon the trigger time, was consistent with a Gaussian fit and accrued 24,972 ± 158 events over a 57,328.04 second interval, resulting in a rate of 0.436 ± 0.003 Hz. Based upon a visual inspection of the light curve, a conservative search window of 40 seconds (beginning at \( T \)) was chosen. Hence, 17.44 ± 0.12 background events (\( n_b \)) were expected on-time in AMANDA-II prior to any quality selection. Signal neutrino spectra were simulated for three models (see figure 1) by propagating a total of \( \sim 440,000 \) muon neutrinos (\( \nu_\mu + \bar{\nu}_\mu \)) from an error box in the sky defined by the spatial localization of the radio afterglow (see table 1). Event quality selection was optimized for the best limit setting and discovery potential by minimizing the
model rejection factor (MRF) \[11\] and the model discovery factor (MDF) \[12\], respectively. Although multiple observables were investigated, a single criterion emerged, based upon the maximum size of the search bin radius (Ψ), i.e. the space angle between the reconstructed muon trajectory and the GRB’s position.

Our search, optimized for 5σ discovery (requiring 4 events within Ψ ≤ 11.3°), is consistent with a null signal. Upper limits, summarized with our results in table 2, do not constrain the models tested using AMANDA-II. Effective neutrino and muon areas are given in figure 5. The number of expected signal events in IceCube (Ns) for model 1 is consistent with \[13\], when neutrino oscillations are considered. For model 3, our results for Ns are in agreement with \[9\] and \[14\], when one adjusts for the assumptions of \[7\]. Selection based upon Ψ was robust across the models tested in AMANDA-II, as illustrated in figure 2. However, the MRF/MDF and hence the limit setting/discovery potential was strongly model dependent, varying by over an order of magnitude for models 1 and 3. Furthermore, using the same theoretical framework, the response of AMANDA-II and IceCube to spectra based upon discrete and average parameters are discrepant in mean neutrino energy and event rate by over an order of magnitude as illustrated in figure 1 and table 2. Such variance in detector response unequivocally demonstrates the value of a discrete modeling approach when making correlative neutrino observations of individual GRBs, especially in the context of inferred astrophysical constraints, in agreement with \[9\].

### Table 2. Summary of Results for GRB030329. Primes indicate value after selection for IceCube (Ns) and AMANDA-II (nb). Superscripts indicate A=MRF and B=MDF optimization. Average upper limit (sensitivity) and flux upper limit values are given for AMANDA-II. The effects of neutrino flavor oscillations have been included.

| Neutrino Flux Model Φνµ | Search Bin Radius ΨA, ΨB | Background Expected in AMANDA-II nA, nB | Expected Number of Neutrino Events in AMANDA-II Nν, nA, nB | Observed Events in AMANDA-II nobsA, nobsB | Optimization Method for AMANDA-II MRF, MDF | Average Upper limit \(\frac{dΦ}{dΩ}\) [Sensitivity] GeV cm\(^{-2}\) s\(^{-1}\) | Flux Upper Limit \(\frac{dΦ}{dΩ}\) GeV cm\(^{-2}\) s\(^{-1}\) |
|-------------------------|--------------------------|----------------------------------------|------------------------------------------|-------------------------------------|---------------------------------|--------------------------------|--------------------------------|
| 1                       | 21.3, 11.3               | 17.44, 0.23, 0.06                      | 0.1308, 0.0202, 0.0156                  | 15, 0                               | 152, 424                        | 0.157                          | 0.150                          |
| 2                       | 18.8, 11.3               | 17.44, 0.17, 0.06                      | 0.0691, 0.0116, 0.0092                  | 15, 0                               | 256, 716                        | 0.041                          | 0.039                          |
| 3                       | 18.5, 11.3               | 17.44, 0.17, 0.06                      | 0.0038, 0.0008, 0.0006                  | 15, 0                               | 3864, 10794                     | 0.036                          | 0.035                          |

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Figure 1. Upper panel - Prompt neutrino energy flux for models 1 (solid black), 2 (dashed blue) and 3 (dot-dashed red), based upon equation 2a for GRB030329. Lower panel - Detector response for models 1 (black), 2 (blue) and 3 (red) for AMANDA-II (solid) and IceCube (dashed). Note how the variance in the neutrino spectra (upper panel), due to the variance of electromagnetic parameters used in equation 2a, directly translate into the variance in detector response (lower panel), which exceed an order of magnitude, as manifested in observables such as the expected mean neutrino energy and rate. The effects of neutrino flavor oscillations have been included.
Figure 2. AMANDA-II signal efficiency/background rejection for GRB030329 models 1-3 using MRF (vertical dashed blue, dashed-dot green and dashed-dot-dot red) and MDF (vertical black dotted) optimizations. Both MRF and MDF selections reject $\sim 99\%$ of the background while retaining $\sim 86\%$ and $\sim 77\%$ of the signal, respectively.
Figure 3. Upper panel - The effective muon neutrino area. A peak of $\sim 80$ m$^2$ and $\sim 700$ m$^2$ occurs at $\sim 2$ PeV for AMANDA-II and IceCube, respectively. Lower panel - The effective muon area for energy at closest approach to the detector. At $\sim 200$ TeV, the effective muon area for IceCube, $\sim 1$ km$^2$, exceeds that of AMANDA-II, $\sim 100,000$ m$^2$, by an order of magnitude. For both panels, MDF optimized AMANDA-II results for models 1 (dashed black), 2 (dashed blue) and 3 (dot-dashed red) and predicted IceCube (solid black) curves are illustrated for GRB030329 with $\delta_{J2000} \approx 22^\circ$. 