Analytical formula for temperature dependence of resistivity in p-type 4H-SiC with wide-range doping concentrations

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Temperature dependence of resistivity from 250 to 900 K in p-type 4H-SiC with various doping concentrations (5.8 × 10¹⁴–7.1 × 10¹⁸ cm⁻³) was presented. The resistivity was obtained by the van der Pauw method in samples, whose doping concentrations were precisely determined in our previous work. From the experimental results, coefficients for a fitting formula with polynomial approximation were derived. We confirmed that the fitting formula can accurately estimate the resistivity of p-type SiC with wide-range doping concentrations.

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4H-SiC is a promising semiconductor material for power devices because of its wide bandgap, high critical electric field, and high thermal conductivity. Many studies have been performed to develop SiC power devices and their performance was significantly improved. Aside from power-device applications, SiC devices are being recognized as attractive candidates for integrated circuits that can operate under harsh environmental conditions aiming at exploring Venus, underground drilling, controlling engine combustion, and so forth.

For designing high-performance SiC devices or integrated circuits, the temperature dependence of electrical properties in SiC, such as mobility, carrier concentration, and resistivity, is of importance. The physical properties of n-type SiC have extensively been investigated so far, and those of p-type SiC have also been obtained recently. In our studies, the temperature dependences of hole mobility, hole concentration, and Hall scattering factor were shown by performing Hall-effect measurement on thick p-type SiC epilayers with various doping concentrations. Although the resistivity of p-type SiC can be estimated from these data, it is much more useful to give an analytical expression that describes the temperature dependence of resistivity. In this work, the temperature dependence of resistivity in p-type SiC with various doping concentrations is presented and analytical formulas describing resistivity are given.

Figure 1 shows the temperature dependence of resistivity in p-type SiC obtained by the van der Pauw method from 250 to 900 K. The aluminum (Al) doping concentration ranges from 5.8 × 10¹⁴ to 7.1 × 10¹⁸ cm⁻³ and the compensation ratio of all the samples is below 1% except for the sample with the lowest doping concentration (Al = 5.8 × 10¹⁴ cm⁻³), the ratio of which is about 7%. Experimental details were described in our previous paper. It becomes convenient when an analytical equation is derived for the precise estimation of resistivity in p-type SiC at arbitrary temperatures and doping concentrations. In the case of Si, the temperature and doping dependence of resistivity above 300 K are dominated by the temperature- and doping-dependent mobility because all the dopants in Si are almost completely ionized over 300 K. Thus, using empirical formulas for the temperature- and doping-dependent mobility, the resistivity of Si can be estimated. However, as demonstrated in Fig. 1, the resistivity of p-type SiC strongly depends on the temperature and doping concentration, which is attributed to the large ionization energy of Al acceptors (~200 meV) and complicated carrier scattering mechanisms in SiC.

Thus, it is difficult to create a simple equation or an empirical formula for the fitting. In order to acquire the fitting equation, the dependences of resistivity on the temperature and doping concentration should be considered separately.

Figure 2(a) shows the dependence of resistivity on Al doping concentration at 293, 485, and 900 K. The resistivity of the samples with low doping concentrations (<2.0 × 10¹⁶ cm⁻³) increased at high temperatures because almost all acceptors are ionized, while the mobility decreases due to enhanced phonon scattering. On the other hand, the resistivity of the samples with high doping concentrations...
The black, blue, and red solid lines are fitting curves obtained by the (a) first- and (b) third-order polynomial approximations of Eq. (1).

Fig. 2. (Color online) Dependence of resistivity on doping concentration. The black, blue, and red circles denote the experimental values at 293, 485, and 900 K, respectively. The black, blue, and red solid lines are fitting curves obtained by the (a) first- and (b) third-order polynomial approximations of Eq. (1).

Fig. 3. (Color online) Temperature dependence of the coefficients $a_0$ and $a_1$ in Eq. (1), which are determined by the least-squares method applied to Fig. 2(a). The solid lines indicate the fitting curves obtained from the third-order polynomial approximation of Eq. (2).

$ (>2.0 \times 10^{16} \text{cm}^{-3})$ did not monotonically increase with elevating the temperature because the increase in hole concentration compensates the decrease in mobility. A fitting formula for the doping concentration dependence of resistivity at every measurement temperature can be obtained by assuming polynomial approximation as

$$\log_{10}(\rho/\Omega \text{cm}) = \sum_{i=0}^{m} a_i(T) \times \log_{10}([\text{Al}]/\text{cm}^{-3})^i.$$  \hspace{1cm} (1)

Here, $\rho$ is the resistivity, $a_i$ is the fitting coefficient, $T$ is the absolute temperature, and $[\text{Al}]$ is the aluminum doping concentration. From this equation, fitting curves can be acquired and indicated in Fig. 2(a) with colored solid lines in the case of $m = 1$.

The coefficients $a_0$ and $a_1$ are determined by the least-squares method at individual temperatures and presented in Fig. 3. The absolute values of the coefficients $a_0$ and $a_1$ increase with the temperature, which reflects the increase of the resistivity in the lightly doped p-type SiC ($<2.0 \times 10^{16} \text{cm}^{-3}$) at high temperatures because $a_0$ and $a_1$ represent the intercept and slope of fitting lines, respectively. As mentioned above, the increased resistivity in the lightly doped p-type SiC at high temperatures arises mainly from the decrease in mobility because almost all acceptors are ionized. Hence, both coefficients saturate above 600 K because hole mobility weakly depends on temperature at such a high temperature. The coefficient $a_1$ roughly saturates to minus unity, indicating that resistivity is proportional to the inverse of Al concentration, which is attributed to the complete ionization and the small temperature dependence of the hole mobility at high temperature. By utilizing the coefficients $a_0$ and $a_1$ obtained from the experimental results, the dependence of resistivity on doping concentration can be estimated at each measurement temperatures. However, besides the coefficients at the measurement temperatures, the coefficients at any temperatures should be known to acquire the dependence of resistivity on doping concentration at arbitrary temperatures.

Since the series of data points of the coefficient $a_i$ is affluent, we assume that the coefficient at an arbitrary temperature between 293 and 900 K can be figured out by obtaining an analytical formula for the temperature-dependent coefficient $a_i$. In fact, the temperature dependence of the coefficient can be traced by using a third-order polynomial approximation as

$$a_i(T) = \sum_{j=0}^{n} b_{ij} \times T^j.$$  \hspace{1cm} (2)

Here, $b_{ij}$ is the fitting coefficient for $a_i$ ($n = 3$). Thus, the temperature dependence of the coefficient $a_i$ can be presumed by utilizing $b_{ij}$ values, leading to the determination of resistivity at arbitrary temperatures and doping concentrations.

The $b_{ij}$ values for the fitting coefficient $a_i$ were determined by the least-squares method and are summarized in Table I. The fitting results are indicated in Fig. 3 by black ($a_0$) and red ($a_1$) solid lines, which agreed well with the coefficient $a_i$ obtained by the process mentioned above. From Eqs. (1) and (2), and Table I, the temperature dependence of resistivity at the doping concentrations experimentally investigated can be calculated and several representative curves ($[\text{Al}] = 2.0 \times 10^{15}$ and $3.0 \times 10^{17} \text{cm}^{-3}$) are plotted with colored dotted lines in Fig. 1. All of the fitting curves from 300 to 900 K are in relatively good agreement with the experimental resistivity.
The resistivity of p-type SiC is very sensitive to the temperature. For fabricating a resistor of high-temperature dependent resistivity, the knowledge obtained in this study is significantly important and practical.

The temperature dependence of resistivity in p-type SiC with the doping concentration of 1.7 × 10^{17} cm^{-3} is least dependent on temperature (not shown). Since resistivity with a small temperature dependence is required to design high-temperature integrated circuits, the knowledge obtained in this study is significantly important and practical.

In summary, the temperature dependence of resistivity in p-type 4H-SiC with various doping concentrations (5.8 × 10^{14}–7.1 × 10^{18} cm^{-3}) was presented. The analytical formula of the polynomial approximation for resistivity was derived from the obtained data. The fitting formula enables accurate estimation of resistivity in p-type 4H-SiC with wide-range doping concentrations at arbitrary temperature from 250 to 900 K. This work provides the convenient data and analytical formula for designing SiC devices operating in a wide temperature range.

### Table II. Fitting coefficient $b_i$ for Eq. (2). For the accurate determination of resistivity, the presented values with the significant digit of eight should be input precisely because resistivity is very sensitive to the fitting coefficient $a_i$ in Eq. (1). The applicable ranges of these coefficients for doping concentration and temperature are expanded to $5.8 \times 10^{14}$–7.1 × 10^{18} cm^{-3} and 250–900 K, respectively.

| $j$ | $b_0$ | $b_1$ | $b_2$ | $b_3$ | $b_4$ | $b_5$ | $b_6$ |
|-----|-------|-------|-------|-------|-------|-------|-------|
| 0   | $-3.8715528 \times 10^5$ | $4.2487692 \times 10^{-1}$ | $-1.7998246 \times 10^{-4}$ | $3.8533797 \times 10^{-11}$ | $-4.4873183 \times 10^{-17}$ | $2.7251689 \times 10^{-10}$ | $-6.7889561 \times 10^{-14}$ |
| 1   | $7.0459471 \times 10^2$ | $-7.7583612 \times 10^6$ | $3.3190453 \times 10^{-2}$ | $-7.1547922 \times 10^{-5}$ | $8.4102986 \times 10^{-8}$ | $-5.1587332 \times 10^{-11}$ | $1.2985038 \times 10^{-14}$ |
| 2   | $-4.2406555 \times 10^6$ | $4.6887048 \times 10^{-1}$ | $-2.0156622 \times 10^{-3}$ | $4.3872158 \times 10^{-6}$ | $-5.1997984 \times 10^{-9}$ | $3.2159630 \times 10^{-12}$ | $-8.1685031 \times 10^{-16}$ |
| 3   | $3.8575967 \times 10^{-1}$ | $-9.3826374 \times 10^{-3}$ | $8.6008784 \times 10^{-5}$ | $-8.9006925 \times 10^{-8}$ | $1.0626928 \times 10^{-10}$ | $-6.6243121 \times 10^{-13}$ | $1.6947511 \times 10^{-17}$ |

500 K. Thus, the small $\Delta p / \rho_{RT}$ ratio of p-type SiC in the wide temperature range is unique to p-type SiC, which is attributed to the incomplete ionization of Al acceptors at moderate temperatures. The resistivity of p-type SiC above 500 K with a doping concentration of 6.8 × 10^{18} cm^{-3} is least dependent on temperature (not shown). Since resistivity with a small temperature dependence is required to design high-temperature integrated circuits, the knowledge obtained in this study is significantly important and practical.

Figure 4 shows the temperature dependence of resistivity normalized by the value at 293 K. The symbols denote the experimental data. For fabricating a resistor of high-temperature integrated circuits, temperature-independent resistivity is ideal. The suitable doping concentration can be suggested by utilizing the proposed analytical formula. The black solid line in Fig. 4 is normalized resistivity in p-type SiC with a doping concentration of 1.7 × 10^{17} cm^{-3} derived from the calculation with Eqs. (1) and (2), and Table II. The decrease in mobility at the elevated temperature is most effectively compensated by the increase in hole concentration, leading to the smallest dependence on temperature. The $\Delta p / \rho_{RT}$ ratio is within 35% in the entire temperature region from 300 to 900 K, where $\rho_{RT}$ and $\Delta p$ denote resistivity at 293 K and the difference in resistivity from $\rho_{RT}$, respectively. Although resistivity in a highly doped n-type Si shows a small $\Delta p / \rho_{RT}$ ratio of less than 5%,

Fig. 4. (Color online) Temperature dependence of the resistivity of p-type SiC, which is normalized by the value at 293 K. The symbols are obtained from the experiment. The normalized resistivity of p-type SiC with a doping concentration of 1.7 × 10^{17} cm^{-3} is calculated from Eqs. (1) and (2), and Table II, as indicated by the black line.
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