15 Global properties are drawn from measurements over a large solid angle of the host galaxy. This contrasts with “local” properties that are drawn from a small solid angle around the supernova position (Rigault et al. 2013).
that the light-curve shape parameter is correlated with the host-galaxy morphology. Kelly et al. (2010), Sullivan et al. (2010), Lampeitl et al. (2010), Gupta et al. (2011), and Suzuki et al. (2012) find that Hubble residuals depend on host mass. Konishi et al. (2011) find a similar dependence on metallicity while D’Andrea et al. (2011) and Hayden et al. (2013) find a dependence on both metallicity and specific star formation rate (sSFR).

Childress et al. (2013b, hereafter C13b) perform such an analysis on the supernovae of the Nearby Supernova Factory (SNfactory; Aldering et al. 2002). Supernova distances are derived using linear magnitude corrections based on light-curve shape and color parameters from SALT2 (v2.2.0; Guy et al. 2007, 2010) fits to the SNfactory synthetic photometry, using the procedure described in Bailey et al. (2009); in this article, these linearly corrected distances are referred to as “SALT2” distances. Host mass, sSFR, and metallicity are derived from photometric and spectroscopic observations of the associated galaxies (Childress et al. 2013a, hereafter C13a). Their findings are consistent with previous studies; when splitting the SN Ia sample by the host mass, sSFR, and metallicity at \( \log (M_*/M_\odot) = 10.0, \log (sSFR) = -10.3, \) and \( 12 + \log (O/H) = 8.8, \) respectively, they find that SNe Ia in high-mass (low-sSFR, high-metallicity) hosts are on average \( 0.085 \pm 0.028 \) mag \( (0.050 \pm 0.029 \) mag, \( 0.103 \pm 0.036 \) mag) brighter than those in low-mass (high-sSFR, low-metallicity) hosts after brightness corrections based on the SALT2 light-curve shape and color brightness corrections.

The Hubble residuals depend on the model used to determine the absolute magnitude. Although there is the expectation that the progenitor variability tracked by the host-galaxy parameters must also be directly manifest within the supernova signal itself, it appears that it is not captured by the light-curve models that were used and the associated standardization in the cited work. The SDSS-II Supernova Survey, using samples divided by passive and star-forming hosts, finds Hubble residual biases between both SALT2- and MLCS2k2-determined distances (Lampeitl et al. 2010): indication that the bias from the two light-curve fitters share a common source. The two parameters of one model are highly correlated with the two parameters of the other (Kessler et al. 2009), which brings into question whether a third light-curve parameter associated with host properties is not being captured by SALT2 or MLCS2k2. Although there are searches for such a third light-curve parameter associated with Hubble residual bias (e.g., Hayden et al. 2010, who test whether heterogeneity in light-curve rise times can account for the SDSS-II result), as of yet no such parameter has been found.

Kim et al. (2013, hereafter K13) expand the optical light-curve parameterization by characterizing light curves through the probability distribution function of a Gaussian process for thegressed values at phases \( -10 \) to 35 in one-day intervals relative to peak, rather than the parameters of a best-fit model. The relationship between the K13 light-curve parameters and light-curve shapes can be seen in Figure 4 of K13 and are described briefly here. The effect of the \( \alpha(0) \) parameter on the light curve is relatively phase-independent and is increasingly stronger in bluer bands, which is very similar to the behavior of host-galaxy dust and the color parameters of other fitters. The \( \alpha(1) \) parameter affects the light-curve width and color around peak, similar to the stretch \( (x_1) \) and \( \Delta \) parameters of SALT2 and MLCS. The \( \alpha(2) \) parameter affects peak colors in a fashion inconsistent with dust \((g^{0.25} - i^{0.25}, g^{0.25} - r^{0.25}, \) and \( z^{0.25} - i^{0.25} \) are positively correlated), controls the near-UV light curve width, and influences the light-curve decline 20–30 days after peak brightness. The \( \alpha(3) \) parameter most notably affects peak color and the light-curve shape through all phases of the \( g^{0.25} \) band. The K13 light curve parameters capture the UV light-curve diversity distinct from those of SALT2; Figure 10 shows plots of SALT2 versus K13 light-curve parameters. The absolute magnitude at peak \( B \)-band brightness is taken to be an unknown function of a set of 15 light-curve parameters; after modeling the function as a Gaussian process and training, the absolute magnitude can be determined to have a dispersion as low as 0.09 mag. The larger number of light-curve parameters (and their principal component compression) that reduce the dispersion may be sensitive to the pertinent information encoded in the host-galaxy parameters.

In this article, we look for a dependence of the K13 light-curve parameters and Hubble residuals on host-galaxy parameters. K13 use a supernova data set analyzed in C13b, so the absence of correlations between Hubble residuals and host-galaxy parameters could provide positive evidence for the improved performance of the K13 method with respect to supernova environmental biases.

2. DATA SET

Our sample starts with the 119 SNe Ia from K13. These objects have spectrophotometric data sets obtained by the SNfactory with the SuperNova Integral Field Spectrograph (SNIFS; Lantz et al. 2004) that had been fully processed as of early 2011. The instrument has a fully filled \( 6.4' \times 6.4' \) spectroscopic field of view subdivided into a grid of \( 15 \times 15 \) spatial elements and a dual-channel spectrograph covering 3200–5200 Å and 5100–10000 Å. The median signal-to-noise ratio \((S/N)\) within 2.5 days of peak brightness is 10.2 per 2.4 Å bin. The observing strategy provides observations of each supernova every 2 to 4 days up to \( \sim 45 \) days after the date of maximum light. The spatial information provided by SNIFS enables photometric flux extraction for each spectral resolution element, making the reduced data spectrophotometric (Bongard et al. 2011; Buton et al. 2013). Flux-calibrated multi-band light curves are composed of synthetic photometry that is calculated by integrating spectra over the transmission function of the observer optical griz bands.

We are interested in the light-curve parameters and Hubble residuals of the supernovae analyzed in K13 (the same studied by C13b). The objective of K13 was to calibrate absolute magnitudes at peak brightness based on light-curve shapes and colors. The goal of this article is to examine possible biases in Hubble residuals, not to minimize the dispersion as in K13; we therefore use a different sample selection which increases the number of supernovae used in this analysis to improve the statistics.

The supernova subsamples considered in our analysis are summarized in Table 1. Our full sample requires \( >16 \) points over all bands with \( S/N > 50 \); this ensures temporal coverage to inform the regression of the multi-band light curves from roughly 10 days before to 40 days after the \( B \) maximum light. A \( z < 0.1 \) requirement reduces the sensitivity of the Hubble residuals on the cosmological parameters \( \Omega_M \) and \( \Omega_L \). In K13, SN 13 was identified as having one spectrum that produced synthetic photometry discrepant with the rest of the light curve (see their Figure 3 for the effect). For consistency with K13, we take the very conservative step of rejecting any supernova with at least one synthetic photometry point \( >5\sigma \) away from the
mean regressed light curve that was predicted by the Gaussian process, even though such spectra have already been internally flagged as having processing errors. Only six objects (each with one outlying point), SNe 8, 14, 85, 98, 99, and 111, are thus culled.

The above requirements leave a full sample of 103 supernovae. To ensure that biases are not introduced through extrapolation in the Gaussian process regression, we define the early sample as the subset of 64 supernovae from the full sample with data from at least 2 days before the date of maximum brightness.

In K13, the calibration of absolute magnitudes is trained for the specific rest-frame wavelengths probed by the observation, and several filter sets were considered. The dispersion in Hubble residuals of the validation sample of 43 SNe was smallest for the absolute-magnitude calibration for the \(i\) band of the blueshifted Dark Energy Survey griz filter set, i.e., the rest-frame bands of a supernova at redshift \(z = 0.25\) covered by standard griz, which amount to supernova-frame effective wavelengths of 378, 497, 602, and 708 nm. These filters are annotated with a superscript \(\textgriz} \). As our objective is to see how well SN Ia distances could be calibrated without restricting ourselves to a specific observer filter system, we use this particular training to look for the dependence of light-curve parameters and Hubble residuals on host-galaxy properties. The Hubble residuals are calculated as the difference between the true and inferred peak magnitudes of the Gaussian process model from Table 5 in K13, with the true magnitude being that which was regressed by the light-curve model and the inferred being that which was regressed from the light-curve shape and color parameters. They perform four distinct analyses with different training and validation sets such that each supernova was in a validation set once and only once. For each supernova, the tabulated absolute magnitude is the one inferred while it was part of the validation set; in this work, the Hubble residuals of all supernovae are treated collectively, even though they were not analyzed with the same trained model.

The statistics of interest in this article cannot benefit and in fact suffer from the overtraining of light-curve and absolute-magnitude models that can occur in the training process of K13. Not all supernovae were used in the trainings of the K13 model; “training” subsets were used to specify the supernova model, which in turn were used to predict the absolute magnitudes of independent “validation” subsets. Each absolute magnitude used in the current article was determined while the supernova was in the validation set, i.e., the training did not include the supernova itself. Any overtraining of the training set thus appears as an added source of error in the absolute magnitudes. In the present article, the signals of interest are deviations of Hubble residuals that are correlated with host-galaxy properties; no host-galaxy property information was used in the determination of the absolute magnitudes.

3. SUPERNOVAE WITH DATA COVERAGE OVER PEAK BRIGHTNESS

The early sample is a fair sample with which to examine the K13 analysis and training: supernovae lacking rise-time data extend the Gaussian process regression outside of its expected range of applicability as peak magnitudes would then be extrapolated rather than interpolated. The light curves in extrapolated regions revert toward the mean function (the updated template of Hsiao et al. (2007) in the analysis of K13) and have uncertainties bounded by the Gaussian Process kernel model rather than the data. For this reason, the K13 training sample was restricted to supernovae with data from earlier than two days before the date of maximum.

We look for a correlation between light-curve parameters and the global host-galaxy properties of C13a in the early sample. Note that each property has a different galaxy subset for which there is a measurement; the metallicity measurement in particular requires emission lines and no contamination from active galactic nucleus emission. Figure 1 shows scatterplots from one of the light-curve trainings. The \(x(0)\) light curve parameter is associated with color and exhibits similar trends as the SALT2 \(c\) parameter shown in C13b; larger (redder) values trending with higher mass and metallicity hosts as could be explained by host-galaxy dust absorption or a color–metallicity dependence. The \(x(1)\) parameter is correlated with SALT2 \(x_1\), and a smaller range of \(x(1)\) values in low-mass and low-metallicity hosts is apparent. The \(x(2)\) parameter has a larger color shift compared to \(x(1)\), broadens the post-maximum light curve, and shifts the height and phase of the secondary maximum in \(c_{0.25}\) and \(c_{0.25}\). There are no low \(x(2)\) values in low-metallicity hosts. The \(x(3)\) parameter is anti-correlated with \(x_1\) and is associated with variability in UV light-curve brightness and shape as well as the red secondary maximum. The set of extreme positive \(x(3)\) values are associated with high-mass galaxies.

We use the results of C13b who apply a SALT2 fit and make magnitude corrections on synthetic photometry using observer-frame, non-overlapping boxcar filter functions whose wavelength ranges correspond to Johnson–Cousins B, V, and R. The K13 Hubble residuals are plotted against the SALT2 residuals in Figure 2, with the early sample distinguished with filled symbols. Qualitatively, most of the solid points with SALT2 Hubble residual less than \(-0.1\) have K13 residuals that are closer to zero (they lie above the slope \(= 1\) curve; also compare the skewness from the negative sides of the histograms in Figure 2). The positive correlation between the residuals shows that the two methods are subject to shared “intrinsic dispersion” that is irreducible for both.

Over the entire early sample there is no significant bias between the supernova distances determined by K13 and SALT2: the distribution of the difference between their Hubble

| Sample | Selection Criteria | Number |
|--------|--------------------|--------|
| Initial | SNfactory data fully processed by early 2011 | 119 |
| Full   | \(\geq 16\) photometric points with S/N \(\geq 50\) \(0.015 < z < 0.1\) Removal of SN 13 identified in K13 as having spurious photometry No photometry \(>5\sigma\) from regressed mean | 103 |
| Early  | In full sample Photometry at least two days before B maximum | 64 |

Table 1
Supernova Samples

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residuals has mean $-0.004 \pm 0.010$ mag. However, biases do appear when the early sample is divided by a global host-galaxy property. For each host parameter, the population is split into two samples at boundaries established by previous studies: at $\log (M/M_\odot) = 10.0$ for the host-galaxy mass, $\log (\text{sSFR}) = -10.3$ for the specific star formation rate, and $12 + \log (O/H) = 8.8$ for the metallicity. Not all hosts have measurements of these properties; for the early sample the number of supernovae in the low- and high-bin subsets are (37, 24) for mass, (18, 43) for sSFR, and (18, 21) for metallicity. For the full sample the numbers are (50, 49) for mass, (38, 61) for sSFR, and (30, 32) for metallicity.

The K13 minus SALT2 Hubble residuals in subsets defined by these splits are given in Table 2. The significance of the differences are at 1.6$\sigma$, 1.8$\sigma$, and 2.7$\sigma$ for mass, specific star formation rate, and metallicity, respectively.

The biases in K13 and SALT2 Hubble residuals imply that they should produce different Hubble residual steps. The mean Hubble residual and intrinsic magnitude dispersion are fit for each subset that is defined by the host-galaxy parameters and any significant signal in the mean of the less-than sample minus the greater-than sample (i.e., the Hubble residual step) is an indicator of population dependence. A non-zero slope of a linear fit to the data also indicates dependence.

For the K13 four-band regressed approach, the Hubble residuals and slopes are shown as a function of the host galaxy mass, the specific star formation rate, and the metallicity in Figure 3. The Hubble residual steps and slopes are listed in the Early/gri$^{0.25}$ row of Table 3. The signals for step or slope have significance $<1\sigma$ for all cases except for the slope in sSFR that has a 2$\sigma$ significance. We test for the presence of a significant residual correlated structure that may not be captured in the simple step and slope statistics by assuming an underlying covariance in the Hubble residuals which is described as $|a|k_{\nu3/2}(r; |l|)$ and fitting for $r$ and $l$, where $a$ is a normalization parameter, $l$ the correlation length, $k_{\nu3/2}$ is the Matérn function, and $r$ is the separation in the log galaxy parameter. Probability distribution functions of the covariance parameters are built from the best fits of multiple realizations of sets of points generated based on the data and their uncertainties. In all cases, $a = 0$ falls within less than 1 standard deviation of the mean; the data are consistent with having no correlation.

To examine the influence of wavelength coverage, the light-curve to absolute-magnitude relation is retrained as in K13 using the same filter set but omitting the extreme bands, i.e., for gri$^{0.25}$ data and riz$^{0.25}$ data only. The steps and slopes are listed...
Table 2
Mean Difference Between K13 and SALT2 Hubble Residuals

|                | No Split | log (M/M_☉) | log (sSFR) | 12 + log (O/H) |
|----------------|----------|-------------|------------|----------------|
|                |          | Low (mag)   | High (mag) | Low (mag)      | High (mag)      | Low (mag)     | High (mag)   |
| Early sample   |          | −0.009 ± 0.010 | −0.020 ± 0.013 | 0.011 ± 0.016 | −0.025 ± 0.015 | −0.000 ± 0.010 | −0.024 ± 0.011 | 0.024 ± 0.015 |
| Full sample    |          | 0.001 ± 0.009 | −0.021 ± 0.011 | 0.024 ± 0.012 | 0.006 ± 0.014 | −0.003 ± 0.011 | −0.007 ± 0.010 | 0.018 ± 0.015 |

Table 3
Hubble Residual Steps and Slopes

|                | Offset (mag) | Slope (mag dex⁻¹) | Offset (mag) | Slope (mag dex⁻¹) | Offset (mag) | Slope (mag dex⁻¹) |
|----------------|--------------|-------------------|--------------|-------------------|--------------|-------------------|
| Early          |              |                   |              |                   |              |                   |
| g_(r)_25      | 0.013 ± 0.031| −0.007 ± 0.016    | −0.016 ± 0.033| 0.044 ± 0.022     | 0.010 ± 0.035| −0.042 ± 0.051    |
| g_(i)_25      | 0.020 ± 0.031| −0.023 ± 0.016    | −0.036 ± 0.031| 0.066 ± 0.020     | −0.012 ± 0.037| −0.030 ± 0.060    |
| r_(i)_25      | 0.020 ± 0.037| −0.034 ± 0.018    | −0.049 ± 0.036| 0.086 ± 0.024     | −0.039 ± 0.040| 0.213 ± 0.079     |
| SALT2         | 0.047 ± 0.039| −0.047 ± 0.013    | 0.000 ± 0.040| 0.030 ± 0.015     | 0.048 ± 0.040| −0.126 ± 0.043    |
| Full          |              |                   |              |                   |              |                   |
| g_(riz)_25    | 0.045 ± 0.026| −0.028 ± 0.013    | −0.037 ± 0.027| 0.037 ± 0.014     | 0.029 ± 0.030| −0.068 ± 0.040    |
| SALT2         | 0.095 ± 0.030| −0.047 ± 0.013    | −0.048 ± 0.031| 0.030 ± 0.015     | 0.059 ± 0.032| −0.126 ± 0.043    |
| C13b          |              |                   |              |                   |              |                   |
| SALT2         | 0.086 ± 0.028| −0.043 ± 0.014    | −0.051 ± 0.029| 0.031 ± 0.017     | 0.102 ± 0.036| −0.106 ± 0.046    |

Table 4
Differences in K13 and SALT2 Hubble Residual Steps

|                  | Difference in Hubble Residual Step (mag) | log (M/M_☉) | log (sSFR) | 12 + log (O/H) |
|------------------|----------------------------------------|-------------|------------|----------------|
| Early            |                                        |             |            |                |
| g_(r)_25 - g_(r)_25 | 0.001 ± 0.016                         | 0.019 ± 0.017| 0.013 ± 0.017|                |
| g_(i)_25 - r_(i)_25 | −0.002 ± 0.020                        | 0.028 ± 0.018| 0.041 ± 0.018|                |
| g_(i)_25 - i_(i)_25 | −0.004 ± 0.020                        | 0.012 ± 0.020| 0.026 ± 0.017|                |
| g_(i)_25 - SALT2  | −0.032 ± 0.019                         | −0.025 ± 0.019| −0.048 ± 0.021|                |
| Full             |                                        |             |            |                |
| g_(riz)_25 - SALT2 | −0.046 ± 0.016                        | 0.015 ± 0.017| −0.023 ± 0.018|                |

The host-galaxy-property values used to separate the sample come from published work that searched for systematic biases. The objective of this article is to use the K13 Hubble residuals to probe existing positive detections of bias residuals, not to mine for systematics again. Nevertheless, we check whether a different bias is evident in our sample. Figure 4 shows Hubble residual steps for a range of parameter boundaries; there are no >2σ steps.

4. Expanding the Supernova Sample

Neither the K13- nor SALT2-determined distances of the early sample show significant >3σ Hubble residual steps with respect to host-galaxy properties. We now consider how this subset behaves relative to larger subsets with relaxed criteria for the first phase of SNIFS data. This bridges the results of the early sample with C13b, who used the same data and SALT2 fits from the same parent supernova set to find a step at >3σ with host mass, which was consistent with previous studies (Kelly et al. 2010; Sullivan et al. 2010; Lampeitl et al. 2010; Gupta et al. 2011; Konishi et al. 2011; D’Andrea et al. 2011). Our recalibration of the SALT2 Hubble residual steps for the C13b sample are given in Table 3 as “C13b/SALT2”; the results are consistent with C13b to 0.003 mag, the slight differences being due to our fitting of separate (rather than joint) intrinsic dispersions for each population.

The principal feature that distinguishes the early sample is the requirement for data at least two days before the peak. Here we examine the effect of changing the earliest phase required in the light curves. While the K13 analysis is expected to be biased with underestimated uncertainties for supernovae without data coverage at the peak, this does provide useful insight when bridging the SALT2 results of the early sample with that of the full sample.

as “Early/g_(r)_25” and “Early/r_(i)_25” in Table 3: no significant steps are seen in either of these trainings, but non-zero slopes (at >3σ) are found with sSFR for both. For the r_(i)_25 set in particular, the significance and size of the slope exceeds that of SALT2.

The SALT2 (v2.2.0) Hubble residual steps and slopes are listed as the “Early/SALT2” entry in Table 3. The significance of the mass step is reduced to 1.4σ. Splits in the other host-galaxy properties show a similar weakening of the significance of the step in the two samples.

Differences in the Hubble residual steps from different samples or light-curve analyses are listed for select pairs in Table 4. The steps of the various filter sets are calculated using the same supernovae and data, so their differences and uncertainties are not taken directly from Table 3 but are recalculated independently. A relevant case is the effect of excluding the blueshifted g band at 378 nm; as noted above, the r_(i)_25 fit has a comparatively larger and more significant slope with sSFR than those of other runs.
Figure 3. Hubble residuals of the $griz^{0.25}$-band analysis of K13 applied to the early sample, as a function of the host-galaxy mass $\log (M/M_\odot)$, the specific star formation rate $\log (sSFR)$, and the metallicity $12 + \log (O/H)$. Solid bands show the $\pm 1\sigma$ measurement of the Hubble residual weighted mean for each subset. The solid line shows the best fit, and the dashed lines show the $1\sigma$ range of the linear model.

(A color version of this figure is available in the online journal.)

Figure 5 shows the Hubble residual steps with respect to the host mass as a function of the required phase of first observation, and the number of supernovae from low-mass and high-mass hosts that enter each calculation. We first consider the asymptotic limit where the first phase must be $<9$ days after peak: this unconstraining requirement accommodates all 103 supernovae in the full sample. Table 2 shows that like the early sample, biases between K13 and SALT2 Hubble residuals in the full sample only appear after splitting by the host-galaxy property. K13 and SALT2 Hubble residual steps for the full
Figure 4. Hubble residual steps of the $griz^{0.25}$-band analysis of K13 applied to the early sample, for a range of parameter boundaries for the host-galaxy mass $\log(M/M_\odot)$, the specific star formation rate $\log(sSFR)$, and the metallicity $12 + \log(O/H)$.

Sample are given in the “Full” rows of Table 3. This larger set does have a positive SALT2 mass-step detection at 3.2$\sigma$; the K13 result has a less significant step detection at 1.7$\sigma$. The steps calculated from median Hubble residuals are 0.061 mag and 0.019 mag for SALT2 and K13, respectively, within 1$\sigma$ of the weighted-mean results. Similar trends are seen with sSFR and metallicity. Note that the full sample, with a slightly smaller sample, gives results similar to C13b.

The results of the early sample are (marginally at <2$\sigma$) consistent with those of the full sample. The complement (full–early) sample has a step of 0.181 ± 0.052, so the difference in the steps of the two samples is 0.127 ± 0.064 mag. The step of the early sample is within 1.6$\sigma$ of the full sample using SALT2. The null Hubble residual step evolves into a positive signal with a slight increase in signal and slight decrease of noise. A bias in the SALT2 determination of corrected peak brightness between the early and full samples could be introduced when including or omitting rise-time data. The reapplication of SALT2 on artificial supernovae in the early sample created by removal of early data shifts magnitudes by $-0.010 \pm 0.008$ mag and $-0.005 \pm 0.006$ for low- and high-mass hosts, respectively and a new mass step of 0.040 ± 0.042; this does not account for the 0.048 mag difference between the early and full samples. Samples defined by a more stringent first-phase requirement than the early sample have a small number and a fraction lower than the asymptotic limit of high-mass hosted supernovae. We have performed an extensive search for physical sources of bias between observing start and host-mass: none have been found.
Figure 5. Hubble residual steps in the sample split by host-galaxy mass as a function of required phase of first observation. Each measurement includes the preceding sample of SNe. Blue circles are results for SALT2 and red diamonds for K13. Larger symbols with error bars are steps calculated using the weighted-mean Hubble residuals, whereas the smaller symbols are median Hubble residuals. The dashed line shows zero Hubble residual step between high- and low-mass hosts. The upper bar plot shows the number of supernovae from low-mass hosts (blue) and high-mass hosts (red hatched) included for each phase. The samples representing the early and full samples are indicated with arrows.

Statistics examined include the first-phase versus local surface brightness, supernova magnitude and color at first observation, the SALT2 $x_1$ light-curve shape parameter, and source of the supernova discovery.

For K13, the step in the early sample is within $1.2\sigma$ of that from the full sample. The K13 median steps are consistent with zero over all first-phase requirements.

The criterion for data at least two days before peak for the early sample is based on the selection of K13, fixed before any association with the host-galaxy properties was made. Figure 5 shows that relaxing the criterion to include additional supernovae with coverage before the peak does not affect the Hubble residual step. Three supernovae with K13 Hubble residuals $<-0.29$ mag from high-mass hosts with first data phases between maximum and three days after maximum, are responsible for the disparity between mean and median and the increase in Hubble residual step for both K13 and SALT2.

The differences between the K13 and SALT2 mass steps are calculated and shown in Table 4 for the early and full samples. The correlation between K13 and SALT2 Hubble residuals discussed in Section 3 must be accounted for; the quadratic sum of the two step uncertainties and the simple by-eye comparison of the error bars in Figure 2 overestimate uncertainty. The difference in the K13 and SALT2 mass steps for the early sample is at $1.7\sigma$ and for the late sample $2.9\sigma$, suggesting that the lower mass step of K13 is significant. The probability that the magnitude of the mass step is less for the K13 distances compared to SALT2 distances is 0.954 and 0.998 for the early and full samples, respectively.

Table 5

| $x(0)$ Step (mag) | $x(1)$ Step (mag) | $x(2)$ Step (mag) | $x(3)$ Step (mag) |
|-------------------|-------------------|-------------------|-------------------|
| $0.022 \pm 0.023$ | $-0.064 \pm 0.030$ | $-0.080 \pm 0.030$ | $-0.009 \pm 0.031$ |

5. SALT2 HUBBLE RESIDUAL STEPS WITH K13 PARAMETERS

The differing SALT2 Hubble residual steps of the early and late samples may be more efficiently attributed to some underlying light-curve parameter that is not captured by SALT2 and that is not uniformly represented in the two samples; candidate parameters include those identified in the Gaussian process analysis. In a manner similar to the splitting of samples based on host-galaxy parameters, we now calculate SALT2 Hubble residual steps dividing the full sample by each of the first four K13 parameters; results are given in Table 5 for samples split by $x(0)$ through $x(3)$ in turn. The Hubble residual steps are significant ($>2\sigma$) in samples divided by $x(1)$ and $x(2)$. Hubble residuals as a function of these parameters are shown in Figure 6, which also shows as a point of reference and contrast K13 Hubble residuals as a function of these parameters. The most significant step in K13 Hubble residuals for the same four parameters is $1.3\sigma$. Recall that as noted in Section 3 and seen in Figures 6–9 of K13, the K13 parameters do capture diversity in the UV and the secondary maximum at redder wavelengths that
are not captured in the magnitude corrections using the SALT2 parameters $c$ and $x_1$.

6. REVIEW AND DISCUSSION

Absolute magnitudes for a subset of SNfactory objects determined using a novel regression method and tabulated in K13 are used to measure the dependence of Hubble residuals on global host-galaxy properties. Hubble residual steps with host mass, specific star formation rate, and metallicity are $0.013 \pm 0.031$, $-0.016 \pm 0.033$, and $0.010 \pm 0.035$ mag, respectively: all consistent with no step. The SALT2 Hubble residual step for the same subset is $0.047 \pm 0.039$ mag, consistent with a null step at $1.2\sigma$. As a point of comparison with a previous positive detection, Kelly et al. (2010) use an independent supernova sample and color–stretch magnitude corrections to measure a mass step of $0.11$ mag at $2.3\sigma$. This article’s measurements and their measurements are consistent at the $1.7\sigma$ level using K13 and at $1\sigma$ using SALT2 Hubble residuals. For an expanded sample of supernovae with light curves unlike those in the K13 training, the Hubble residual step with mass is $0.045 \pm 0.026$ mag, which is consistent with a null step at the $8\%$ level. In contrast, the color–stretch corrected magnitude step is $0.095 \pm 0.030$ mag, consistent with the null step at only $0.15\%$. The difference between the K13 and SALT2 mass steps for the full sample has an almost $3\sigma$ significance.

The analysis in this article differs with C13b in sample selection. Expansion of the sample to include supernovae with later first data asymptotically gives significant ($>3\sigma$) SALT2 Hubble residual steps with host-mass but not for K13 Hubble residuals. To examine the difference between the early and full samples, we calculate the difference between the SALT2 mass steps of the early and (full–early) samples to be $0.134 \pm 0.065$, a difference this large has a $4.2\%$ chance of random occurrence. The early and late samples do have different populations of objects, for example, the early sample has a higher ratio of low-mass hosts; however, the difference in relative fraction of high- to low-mass hosts is not statistically significant. We conclude that there is an evolution from null to positive-signal SALT2 Hubble residual steps going from early to full samples but that more statistics are required to determine whether the samples are inherently drawn from different parent distributions. K13 Hubble residual steps also evolve with the sample, but they asymptote at $<2\sigma$ for the full sample.

The analysis in this article also differs with C13b in the inference of supernova absolute magnitude. There is SALT2 Hubble residual dependence on both the K13 $x(1)$ and $x(2)$ parameters at the $>2\sigma$ level (though not meeting the $3\sigma$ standard for a positive detection) that does not appear in K13 Hubble residuals. We conclude that multi-band light curves do convey information about supernova absolute magnitude that is
not captured in SALT v.2.2.0. The sample of supernova used to train SALT2 may have a different supernova population than that of the SNfactory data, and its performance on the results of the ensemble average is expected to improve with retraining using a subset of the SNfactory sample. The GP analysis has an advantage in that it nulls out population effects by having training and validation sets drawn from a common sample. Nevertheless, if SALT2 did capture the diversity of light curves no bias would arise due to differing training and validation populations assuming that systematic changes in absolute magnitude are accompanied with changes in the time-evolving spectral energy distribution.

The continued study of correlations between the host-galaxy properties and Hubble residuals is of importance even as tools that measure distances improve. Correlations serve as important diagnostics of potential biases related to progenitor population that are not captured by light-curve parameters or absolute magnitude inference. Better accuracy can be achieved from local host-galaxy properties extracted from the region around the supernova (Rigault et al. 2013), which can give a more accurate view of the progenitor environment compared to global properties.

Physically, there is the expectation that multi-band light curves with broad wavelength coverage transmit information about the progenitor system. Because of limitations in current light-curve fitters, some of this information has only been noted indirectly through host-galaxy properties. This article shows that the novel light-curve analysis of K13 may be capturing more aspects of SN Ia diversity. Application of the method to more supernovae will provide better statistics to test this hypothesis.

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