INTRODUCTION

Rapid population growth and industrialization have elicited unprecedented global water and energy demands (1). Inextricably linked, water production and energy generation processes could benefit tremendously from the development of separations materials with single-solute selectivity (2). Polymeric membranes with subnanometer pores represent a highly practical class of materials for achieving these design goals (3). For water treatment purposes, ultrasel ective membranes can enable precise control over the makeup of permeate and brine streams for complex feed solutions. This level of control could enable more sustainable water treatment by tailoring the treatment to the desired end use and would substantially reduce chemical and energy consumption, ultimately lowering the treatment cost for water production (3, 4). In addition, fit-for-purpose membranes could improve resource recovery efforts (e.g., lithium recovery), sensor devices, and proton selectivity in fuel cells and water electrolyzers (3).

Biological channels, such as the potassium (K⁺) channel, epitomize solute selectivity. By offering a subnanometer environment tailored for K⁺, potassium channels can offset the energy-intensive dehydration process induced by extreme confinement, allowing K⁺ to transport >10⁴ faster than similar cations such as sodium (Na⁺) (5, 6). Incorporating ion-selective channels or ligands in polymer matrices to mimic the selective behavior of biological channels has gained recent interest (7). This technique remains unproven, however, with experimental performance falling far below conventional polymeric and biological membranes due to fabrication-induced defects (2, 8). New and innovative approaches, which require a deeper understanding of fundamental structure-property-performance relationships in polymeric membranes, are thus imperative for designing solute-tailored selectivity.

Various ion-specific properties can influence ion transport and, hence, ion selectivity. The hydration energy (9–11), charge density (12), and size of an ion have conventionally been considered to play critical roles in ion transport (9, 12, 13). The relative importance of each property toward selective transport, however, remains largely clouded. Our poor understanding of the mechanisms that govern ion-ion selectivity in membranes is, in part, the result of inadequate performance metrics. Ion transport in most salt-rejecting membranes is characterized by the observed rejection. Not only is this an operationally dependent metric, but it also fails to capture the thermodynamics necessary for elucidating important molecular interactions (14). In addition, the conventional Edisionian approach to studying selective transport is often incapable of deconvoluting strongly coupled transport mechanisms. This approach largely relies on elucidating transport phenomena from correlations between ion permeability and singular membrane modifications that are often characterized by only a few physical measurements. The sensitivity of polymeric membranes to their environment, which is evidenced by their anomalous ionization behavior (15), and the complex, inhomogeneous nature of their cross-linked networks restricts the insight of these analyses.

In this work, we comprehensively assess the role of monovalent anion- and membrane-specific properties in overall salt transport. Our analysis focuses on the separation of a wide array of anions of monovalent sodium-based salts by a nanoporous cellulose acetate (CA) membrane to elucidate phenomenological differences in selectivity originating from the anions. We identify the limited role of bulk solvation characteristics while highlighting the critical need to consider entropic barriers when holistically studying ion transport. We combine our experimental data with properties describing ion and ion-membrane interactions, generated from first-principles simulations in this study and obtained elsewhere, for advanced statistical analysis using machine learning techniques to determine the

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most important features for predicting thermodynamic barriers to transport. Notably, we observe entropy-enthalpy compensation (EEC) in the transport thermodynamics, largely influenced by ion-membrane interactions under confinement. Although our results are specific to the membrane used in this study, the reported findings demonstrate a new approach for studying ion transport across all nanoporous polymeric membranes.

RESULTS
 Bulk ion solvation: An inadequate descriptor for ion-ion selectivity

Partial or complete shedding of an ion’s solvation shell, termed “dehydration,” has been proposed as a universal mechanism for ion selectivity in rigid two-dimensional (2D) nanoporous systems (16). Previous studies of nanoporous polymeric systems frequently relate ion hydration energy, \( \Delta G_{\text{Hyd}} \), which describes the energy released when an ion undergoes solvation (17), to the ability of an ion to dehydrate into a confined environment (10–12). Hence, ions with high \( \Delta G_{\text{Hyd}} \) are considered to have strong solvation shells that are not easily shed. That is, ions with high \( \Delta G_{\text{Hyd}} \) incur a substantial energetic penalty for dehydrating, making dehydration unfavorable. The use of \( \Delta G_{\text{Hyd}} \) as a standalone metric for assessing dehydration-limited ion permeation is suspect, however, and has been criticized for its failure to account for other solvation properties that have been shown to influence dehydration, such as the hydrated radius (\( r_{\text{Hyd}} \)). Anisotropy is not reliably captured by \( r_{\text{Hyd}} \), as \( r_{\text{Hyd}} \) is a time-averaged value estimated for a sphere. Alternatively, the ion-water binding energy (\( \Delta G_{\text{B}} \)), which describes the interaction strength of a single water molecule with the ion, can be used to characterize the effect of anisotropic ordering on solvation strength (22). By applying first-principles molecular dynamics (FPMD) simulations (see Materials and Methods) to compute the hydrogen-bonding probability density functions (H-bonding PDFs)

![Fig. 1. Assessing bulk ion solvation as a primary metric for ion selectivity in nanoporous membranes.](image)

Fig. 1. Assessing bulk ion solvation as a primary metric for ion selectivity in nanoporous membranes. (A) Permselectivity of all 18 anions investigated compared to their hydration energies, \( \Delta G_{\text{Hyd}} \) (table S1). All hydration energies used in this analysis were obtained from (17). (B and C) 2D projection distributions of water hydrogens surrounding (B) chloride, Cl\(^-\), and (C) hypochlorite, ClO\(^-\), ions. The scale bar represents the normalized density of water hydrogens, where the values correspond to the percentage probability of finding a hydrogen per square nanometer. (D) H-bonding probability density functions (H-bonding PDFs) for Cl\(^-\), and the chlorine (Cl) and oxygen (O) atoms in ClO\(^-\).
between water molecules and ions, we visualize the effect of anisotropic ordering (Fig. 1, B and C). Specifically, we compare the 2D projection distributions of water hydrogens surrounding Cl\(^-\) and ClO\(_3\)\(^-\), which illustrate how nonuniform electrostatic potentials result in the severe asymmetric solvation of ClO\(_3\)\(^-\) as water molecules preferentially bind to the oxygen atom (Fig. 1D).

As evidenced in Fig. 1 (B to D), anisotropic solvation produces stark differences in the solvated structure of an ion. We thus extend our FPMD simulations to the entire chlorate series (Fig. 2A) to investigate the role of anisotropic solvation in ion selectivity. The bond distance and intensity loosely represent the ion solvation strength. We used the H-bonding PDFs to calculate \(\Delta G_{\text{Hyd}}\), and we computed \(\Delta G_B\) and \(\Delta G_{\text{Hyd}}\) using density functional theory (DFT; see Materials and Methods) for chloride (Cl\(^-\)), hypochlorite (ClO\(^-\)), chlorite (ClO\(_2^\cdot\)), chlorate (ClO\(_3^\cdot\)), and perchlorate (ClO\(_4^\cdot\)), which can be found in Fig. 2B. The trend in simulated \(\Delta G_{\text{Hyd}}\) (ClO\(^-\) > ClO\(_2^\cdot\) > Cl\(^-\) > ClO\(_3^\cdot\) > ClO\(_4^\cdot\)) differs slightly from \(\Delta G_{\text{Hyd}}\) values reported by (17), in which the \(\Delta G_{\text{Hyd}}\) of ClO\(_2^\cdot\) was larger than ClO\(_4^\cdot\).

Despite being interrelated properties, the trend for \(r_{\text{Hyd}}\) (ClO\(_4^\cdot\) > ClO\(_2^\cdot\) > ClO\(_3^\cdot\) > Cl\(^-\) > ClO\(_4^\cdot\)) differs substantially from that of the simulated \(\Delta G_{\text{Hyd}}\) due to shape effects and ionic size (Fig. 2B). \(r_{\text{Hyd}}\) can instead be readily described by the number of water molecules that coordinate with the anion (fig. S1A). \(\Delta G_B\) follows the same trend as \(\Delta G_{\text{Hyd}}\) (fig. S1B), but the two are not perfectly correlated \((R^2 = 0.86)\) because of the added influence of anisotropic water ordering present in \(\Delta G_{\text{Hyd}}\).

We assess the quality of \(\Delta G_B\) and \(r_{\text{Hyd}}\) as rate-limiting predictors for anion permeation by quantifying the change in the fit accuracy (i.e., \(R^2\) value) for permselectivity relative to \(\Delta G_{\text{Hyd}}\) (Fig. 2C). This analysis was only done with the values simulated by FPMD for ions in the chlorate series. We believe the chlorate series is a suitable analysis was only done with the values simulated by FPMD for ions in the chlorate series. We believe the chlorate series is a suitable system, as this set of anions has been extensively used to explain dehydration-limited ion transport, was a far worse predictor for permselectivity than \(\Delta G_{\text{Hyd}}\) \((\Delta R^2 = -75.4\%)\). Collectively, our analysis highlights that bulk solvation properties are poor descriptors for the rate-limiting step in anion transport across polymeric membranes. This likely stems from the inability of bulk solvation properties to adequately account for extrinsic factors that can influence dehydration, such as compensatory ion-membrane interactions (3).

### Energetic barriers: The critical role of entropy

The inability of bulk solvation properties to describe anion permselectivity or dehydration necessitates a more fundamental thermodynamic view of transport (thermodynamic parameters detailed in table S2). Ion solvation in water is enthalpically favorable and entropically unfavorable (17). The process of dehydration is therefore often thought to take the reverse. However, this logic fails to consider the confined system that the ion is dehydrating into. While removing an ion from bulk water increases the entropy of water, previous theoretical work has observed a corresponding decrease in the system’s entropy as the ion permeates the channel, making entropy the major contributor to the permeation barrier (23). A balance is also often struck between entropy and enthalpy for steric and diffusive hindrance factors (discussion in fig. S2).

We approximate the energetics of dehydration into our nanoporous membrane for several anions (Fig. 3A). This is accomplished with empirically derived equations (17) that estimate the transfer energy \((\Delta G^\infty)\) and enthalpy \((\Delta H^\infty)\) associated with ions dehydrating into a nonaqueous solvent (details in fig. S3). Given the marked change in the physical and electrical properties of water confined below 2 nm (24, 25), we can assume that confined water represents a nonaqueous solvent (table S3). Our results indicate that entropic barriers play a predominant role in dehydration as they account for over half of \(\Delta G^\infty\) for all anions examined except thiocyanate (SCN\(^-\)). Entropy should thus be accounted for if dehydration, and the energetics thereof, is to be considered a rate-limiting mechanism for anion permeation. We also find that uncommonly used ionic properties for interpreting ion dehydration, such as molar refractivity

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**Fig. 2. Role of anisotropic solvation in ion selectivity.** (A) FPMD simulations of ion solvation. 3D rendering of solvation shells for several ions in the chlorate series (top) provides a qualitative view of anisotropic ion solvation. Oxygen, hydrogen, and chlorine atoms are represented by red, blue, and cyan colors, respectively. These 3D renderings are based on the PDF of H bonds forming between water molecules and the ions of interest (bottom). (B) Calculated solvation properties of ions in the chlorate series, determined from FPMD simulations (see Materials and Methods). (C) Improvement of the linear regression fit, defined as the normalized increase or decrease in the \(R^2\) value from the linear regression with \(\Delta G_{\text{Hyd}}\) for describing the permselectivity of ions in the chlorate series based on ion-water binding energy \((\Delta G_B)\) or \(r_{\text{Hyd}}\).
and softness, may influence dehydration (details in table S4 and fig. S4).

Our analysis suggests that enthalpy alone cannot reasonably describe anion dehydration, partitioning, or diffusion processes. This explains the limited success and inconsistencies associated with using activation energy, $E_a$, as a descriptor for transport (fig. S5) (12), which is directly related to enthalpy (26). We therefore applied transition-state theory (TST) to relate water-salt selectivity to the free energy barrier, $\Delta G^\ddagger$ (see Materials and Methods). While our measurements are of the entire salt, relative changes in $\Delta G^\ddagger$ are solely attributable to the anion due to all salts being sodium based (27). To use Eq. 2, which links TST to diffusive permeation (26), we isolated the role of advective transport (details in figs. S6 to S9). Although present, advection (i.e., ion transport mediated by fluid flow) did not influence differences in anion permeability or $\Delta G^\ddagger$ (figs. S8 and S9).

The intrinsic correlation between perme selectivity and $\Delta G^\ddagger$, which spans from 34.2 to 42.5 kJ mol$^{-1}$ (Fig. 3B), allows us to reliably extract meaningful entropic, $T\Delta S^\ddagger$, and enthalpic, $\Delta H^\ddagger$, barriers for anion permeation (Fig. 3C). Notably, $\Delta G^\ddagger$ does not mirror $\Delta G^\ddagger$. This suggests that dehydration does not solely govern ion transport in this system, which is likely due to an observed EEC effect: Anions with high entropic barriers (i.e., more negative $T\Delta S^\ddagger$) experience relatively small enthalpic resistance and vice versa. EEC is a common occurrence in selective ion-liquid associations (28, 29). Enthalpically favorable ion-membrane interactions can help reduce $\Delta G^\ddagger$ (3). However, these interactions are met with a corresponding loss of entropy in the form of reduced degrees of translational and rotational freedom (28). This trade-off likely gives rise to the EEC observed in Fig. 3C, which is, to the best of our knowledge, the first report of EEC for ion transport across membranes.

**Relative role of molecular-level features in transport**

Describing ion transport holistically necessitates multiple feature types that capture all relevant ion and ion-membrane interaction properties. We obtained feature data from (i) DFT calculations conducted in this study (see Materials and Methods), (ii) cheminformatics (CI) descriptors from the open-source toolkit, RDKit (30), and (iii) previously published works. DFT calculations and CI descriptors inform the electronic and structural properties of the ion, respectively. DFT is further extended to compute interaction properties between the ion and the membrane material. Macroscopic properties collected from previously published works include commonly used variables important to transport, such as the diffusion coefficient (26), which may not be adequately described by DFT or CI. This extensive data collection resulted in 126 features (tables S5 to S8) that were classified into eight qualitative categories related to ion or ion-membrane interaction properties (Fig. 4A). Categorical mapping was designed to highlight the collective role of strongly interrelated properties and avoid overinterpreting the physical meaning of individual features selected for a small sample set (31, 32).

The linear regression models were trained for $\Delta H^\ddagger$, $T\Delta S^\ddagger$, and $\Delta G^\ddagger$ (Fig. 4, B to D). Feature-selected subsets were obtained with recursive feature addition (RFA; see Materials and Methods). The low mean absolute errors (MAEs < 10%) from RFA are a significant improvement over those obtained from the regularized linear regression (see Materials and Methods) used for comparison. The MAE for the $\Delta G^\ddagger$ model (Fig. 4D) is almost twofold larger than the MAEs for the $T\Delta S^\ddagger$ and $\Delta H^\ddagger$ models. This is largely due to the outlier, tetrafluoroborate ($\text{BF}_4^-$). Removing $\text{BF}_4^-$ would decrease the MAE of the $\Delta G^\ddagger$ model to 3.71%. $\text{BF}_4^-$ may behave as an outlier due to its anomalous chemical behavior (33). This could also likely be due to poor extrapolation by the $\Delta G^\ddagger$ model given that $\text{BF}_4^-$ has the lowest $\Delta G^\ddagger$ value (34.23 kJ mol$^{-1}$). Nonetheless, the decent predictive capability of the models indicates that model feature importance is predictive of design principles.

Both $T\Delta S^\ddagger$ and $\Delta H^\ddagger$ rely strongly on the absolute coefficients (B) from ion structure, accounting for 21.1 and 30.2% of the total feature importance, respectively (Fig. 4, E and F). Macroscopic features selected for $T\Delta S^\ddagger$ (e.g., molecular weight) are also highly correlated with ion structure, increasing the cumulative role of ion structure in $T\Delta S^\ddagger$ to 38.2%. Ion-membrane interactions under confinement are the most important feature category for $T\Delta S^\ddagger$ ($\beta \sum \beta = 45.3\%$). The outsized importance of interaction properties corroborates our physical interpretation of EEC, favorable interactions between the
Fig. 4. Elucidating the molecular features that influence anion transport thermodynamics. (A) Schematic representation of data sourcing 126 features from CI, DFT simulations, and literature (left) and classifying them by qualitative categories related to ion or ion-membrane interaction properties in bulk or confined water (right). Macroscopic properties (M) represent measured values from literature that can indirectly relate to any of the other categories, occasionally overlapping several. (B to D) Accuracy of machine learning for anion (B) $\Delta H^\pm$, (C) $T\Delta S^\pm$, and (D) $\Delta G^\pm$ models. Accuracy is measured by the MAE. $\Delta G^\pm$ predictions for $N_\text{3}^-$ and $SO_4^{2-}$ are displayed as gray diamonds in (D). (E to G) Relative makeup (i.e., % contribution) of qualitative feature categories for anion (E) $\Delta H^\pm$, (F) $T\Delta S^\pm$, and (G) $\Delta G^\pm$ models. $\Delta H^\pm$, $T\Delta S^\pm$, and $\Delta G^\pm$ models consist of 11, 11, and 5 total features, respectively. Two "(M)" labels were provided in (E) to highlight that the macroscopic properties selected were related to polarizability and interaction properties.

The apparent equivalence of the EEC trade-off results in an almost net-neutral output, where $\Delta G^\pm$ varies by only $\sim$8 kJ mol$^{-1}$ despite $T\Delta S^\pm$ and $\Delta H^\pm$ each spanning a range of roughly 40 kJ mol$^{-1}$ between all anions (Fig. 3, B and C). Similar EEC behavior has been observed in biomolecular ligand recognition (29). This behavior, sometimes termed the “window effect,” may be the consequence of the transport process having a finite heat capacity and could explain the limited role of interaction properties in determining overall ion transport (Fig. 4G) (36). Ion electrostatics are instead the most important feature category for $\Delta G^\pm$ ($\beta/\sum \beta = 75.3\%$). Although the anions studied here have the same formal charge, the importance of electrostatics in ion selectivity may stem from the influence of nonuniform charge distributions across polyatomic ions, which are critical to molecular interactions, such as hydrogen bonding or dehydration (21, 37). Confined ion-membrane interactions and polarizability account for 19.7 and 4.9% of the total feature importance, respectively. The strong correlation between $\Delta G^\pm$ and permselectivity (Fig. 3B) signifies that these features are critical for distinguishing anions during selective transport. Notably, bulk solvation properties were not selected as important features for $\Delta G^\pm$. 

ion and CA coincide with entropy loss from reduced degrees of freedom in the membrane. This effect is compounded by the ionic structure, whose shape and size can further complicate the ion’s ability to contort and translate across the dense polymer network (14).

Cumulative ion-membrane interaction properties (i.e., interaction properties in bulk, under confinement, and those from macroscopic features) are also found to be important for $\Delta H^\pm$ ($\beta/\sum \beta = 27.3\%$). The parallelism between $T\Delta S^\pm$ and $\Delta H^\pm$ model features corresponds to the EEC effect observed in Fig. 3C. However, $\Delta H^\pm$ is influenced by ion polarizability ($\beta/\sum \beta = 36.1\%$) substantially more than $T\Delta S^\pm$ is ($\beta/\sum \beta = 6.5\%$). The selection of ion polarizability indicates that dehydration mechanisms are important as ion polarizability indirectly describes an ion’s response to the environment permittivity and its ability to dehydrate into other media (additional discussion in the Supplementary Materials (17)). It has also been shown previously that this parameter is paramount for understanding ion transport across organic-water interfaces (34). The shedding and reorganization of water molecules during dehydration or binding interactions have been suggested as a ubiquitous source for EEC in water-mediated processes (35).
DISCUSSION
Despite recent optimism surrounding the use of TST to understand the molecular mechanisms of solute transport in membranes from an entropy and enthalpy perspective (3), we find that EEC may limit this possibility. Entropy and enthalpy are intricately intertwined. The compensation between the two can complicate the interpretation of thermodynamic signatures, consequently obscuring the physics underlying the observed data (29). Therefore, determining the appropriate membrane modifications and design approach to tailoring ion selectivity is not straightforward. Previous studies have called for using insight from EEC to guide ligand design (38, 39), but this strategy has demonstrated limited utility (29). Our results show that designing membrane channels and matrices from a free energy perspective is more suitable for achieving ion selectivity in nanoporous membranes.

Further, we find there are more important components that influence free energy barriers during ion permeation. In particular, the relationship between the pore and the ion electrical properties is critically important, despite the relatively uncharged nature of the CA membrane (40). The implications of this finding may extend to membrane design. Given the observed importance of electrostatics for predicting \( \Delta G^\ddagger \), we postulate that increasing the charge density of the membrane may enhance its ion-ion selectivity. This relies on the assumption that increasing the charge density would not substantially alter the steric environment of the membrane via excessive swelling. However, a trade-off between ion-ion selectivity and charge density likely exists, as was found between water-salt selectivity and permselectivity (38, 39), but this strategy has demonstrated limited utility (29). Our results show that designing membrane channels and matrices from a free energy perspective is more suitable for achieving ion selectivity in nanoporous membranes.

We interpolated a monovalent anion not used in the training set (azide, \( \text{N}_3^- \)) to further assess the predictability of the \( \Delta G^\ddagger \) model. The predicted \( \Delta G^\ddagger \) (36.45 kJ mol\(^{-1}\)) and permselectivity (\( P_W/P_S = 91 \)) for \( \text{N}_3^- \) coincide extraordinarily well with its measured values: 36.51 ± 0.26 kJ mol\(^{-1}\) and 92 ± 9, respectively (table S10). This finding corroborates the predictability implied by its low MAE and suggests our model successfully captures the critical features for differentiating monovalent anion transport. We extended our interpolation to sulfate (\( \text{SO}_4^{2-} \)) to assess the model’s predictability beyond monovalent anions. The predicted \( \Delta G^\ddagger \) of \( \text{SO}_4^{2-} \) (36.56 kJ mol\(^{-1}\)) suggests that \( \text{SO}_4^{2-} \) should be able to permeate the CA membrane more readily than \( \text{Cl}^- \) (\( \Delta G^\ddagger = 37.76 \text{ kJ mol}^{-1} \)). However, this is counter to experimental observations, which show \( \text{SO}_4^{2-} \) rejection significantly higher than \( \text{Cl}^- \) in nanoporous CA membranes (41). Expectedly, this signifies that the model can interpolate well but struggles to extrapolate to new trends it has not yet seen. Adding data for divalent ions will extend the promise of this approach by providing key features that are likely necessary for comparing transport between ions of varying valency, such as the total valence or charge density.

The results and data produced herein are specific to the nanoporous CA membrane investigated in this study. Nonetheless, our findings show that advanced statistical techniques and machine learning can be applied to elucidate molecular mechanisms that govern selective ion transport. These techniques allow for incorporating a wide array of variables rather than focusing on a readily available few. This approach can also provide more insight into the nature of selective transport in complex environments, such as highly cross-linked and inhomogeneous polymer membranes. Our findings represent an essential step toward the ability to design membranes with ultrahigh ion selectivity.

MATERIALS AND METHODS
Materials and chemicals
A CK-series commercial CA nanofiltration (NF) membrane (GE Osmonics, Minnetonka, MN), with a reported molecular weight cutoff of \( \sim 2000 \text{ Da} \), was used for filtration tests. To abate experimental variation from roll-to-roll processing variability, all CA membranes tested in this study were produced from the same batch (lot no. 3CK00009). The membranes were received as flat sheet samples and were gently washed with deionized (DI) water to remove any preservatives. Membranes were stored in DI water at 4°C. All sodium-based monovalent salts (≥99%) used for anion rejection tests were purchased from Sigma-Aldrich (St. Louis, MO).

Membrane characterization
The average pore size of the NF membrane was estimated by the hindered transport model, which accounts for steric exclusion and hindered convection and diffusion of neutral organic solutes (42). We used erythritol, xylose, and dextrose (≥99%; Sigma-Aldrich, St. Louis, MO) as neutrally charged, low–molecular weight organic tracers (43). Before testing, CA membranes were compacted in DI water under 12.1 bar of hydraulic pressure for 12 hours. After compaction, 50 mg liter\(^{-1}\) as total organic carbon (TOC) of the organic solute was circulated in the membrane system. Permeate samples were collected at 1.38, 4.14, 6.89, and 9.65 bar of applied pressure with a crossflow velocity of 21.4 cm s\(^{-1}\) and a feed solution temperature of 25.0° ± 0.5°C (fig. S10A). The permeate samples were taken after the system was allowed to equilibrate for 30 min at each pressure. Solute rejection was determined by analyzing permeate and feed samples for TOC (TOC V-CSH, Shimadzu Corp., Kyoto, Japan). Further details on the pore size estimation can be found in the Supplementary Materials.

The asymmetric structure of the membrane cross sections was characterized by scanning electron microscopy (SEM; SU-70, 5 kV, Hitachi, Tokyo, Japan) (fig. S10B). Samples were sputter coated with 2 nm of iridium (208HR Sputter Coater, Cressington, Watford, UK) to improve sample conductivity during SEM. Images were captured at ×1200 magnification.

NF system and anion rejection experiments
A custom-built three-cell bench-scale filtration system operating in crossflow mode with a flat sheet membrane cell was used for salt rejection and water permeability tests (fig. S11). The crossflow velocity and effective membrane surface area were 21.4 cm s\(^{-1}\) and 20.0 cm\(^2\), respectively. Retentate and permeate were recirculated between the feed tank and the membrane cells. Before filtration experiments, membranes were compacted in DI water under 12.1 bar of hydraulic pressure for 12 hours. Unless stated otherwise, all filtration experiments were performed with an applied inlet pressure of 6.89 bar to avoid compaction effects that may influence membrane performance. Pure water permeability was determined with
only DI water circulating in the system. The feed solution temperature was kept constant at 22.0 ± 0.5°C during compaction and pure water filtration experiments. Feed solution temperature was varied for anion rejection experiments from 16° ± 0.5°C to 34° ± 0.5°C at 6°C increments. All experiments were operated at pH 5.8, excluding those conducted with sodium hypochlorite (NaOCl) and sodium bicarbonate (NaHCO₃). Filtration experiments with NaOCl and NaHCO₃ were carried out at pH 9 and pH 8.4, respectively, to ensure monovalent anionic speciation. Permeate and feed samples were collected after the system was allowed to equilibrate for 30 min.

Observed salt rejection (Robs) was determined by comparing the salt concentration in the feed (Cf) and permeate (Cp) solutions (Robs = 1 − Cf/Cp). We used a Cf of 2 mM for all filtration experiments. Salt flux (Jw, in moles per square meter per hour) across the membrane was determined by coupling the measured water flux (Jw, in L m⁻² h⁻¹) with Cw (Jw = JwCw). By considering the concentration difference across the membrane, we can extract the salt permeability coefficient, B, in (L m⁻² h⁻¹), from the relation B = Jw/DCm. Here, DCm is the difference in the salt concentration between the permeate and feed-side membrane surface, which can be determined by accounting for concentration polarization in the diffusive boundary layer (details in the Supplementary Materials).

The intrinsic water/salt permeselectivity (Pw/Ps) is an inherent material property (i.e., it is operation independent) that was used to compare the ability of the membrane to discriminate the various ions investigated in this study (4, 40)

\[
P_w = \frac{R_g T}{\bar{\nu}_w (1 - R_w)} \left[ \frac{R_o \exp \left( \frac{\nu}{R} \right)}{\Delta P - \Delta \gamma \exp \left( \frac{\nu}{\delta} \right)} \right]
\]

where Rg, T, and \( \bar{\nu}_w \) are the ideal gas constant (83.145 cm³ bar K⁻¹ mol⁻¹), absolute temperature (298.15 K), and molar volume of water (18 cm³ mol⁻¹), respectively. The driving force is described by the difference between the applied hydraulic pressure (ΔP, bar) and transmembrane osmotic pressure (Δπ, bar). A value of 100 liters m⁻² hour⁻¹ was assumed for the overall feed-side mass transfer coefficient (k) and the feed-side mass transfer coefficient for the solute of interest (k_w) (4).

**Measurement of anion transport energetics**

Transport energy barriers were assessed using TST, which describes a rate constant (k, second⁻¹) in terms of entropic (\( \Delta S^T \)) and enthalpic (\( \Delta H^T \)) barriers (i.e., activation energies) and can be extended to solute permeability (3, 26, 44)

\[
k = B \left( \frac{\delta}{\lambda_m^2} \right) = k_B T \exp \left( \frac{\Delta S^T}{R} \right) \exp \left( \frac{\Delta H^T}{RT} \right)
\]

where \( \delta \) is the membrane thickness (in meters), \( \lambda_m \) is the average distance between energy minima (in meters) as permeating molecules hop between sites within the membrane (details in the Supplementary Materials), k is the transmission coefficient (assumed as unity (44), \( k_B \) is the Boltzmann constant (1.381 ×10⁻²² J K⁻¹), and h is the Planck’s constant (6.626 ×10⁻²³ J s). The entropic barriers are accessible by taking the y intercept of the linearized form of Eq. 2 (3). Similarly, enthalpic barriers are determined from the slope of the linearized equation and can be related, in principle, to the Arrhenius activation energy, \( E_a \), by a factor of RT (i.e., \( E_a = \Delta H^T + RT \)) (26).

**FPMD simulations**

We carried out FPMD simulations to probe the bulk solvation properties of ions in the chlorate series. Specifically, all solutions were modeled by periodic cubic cells consisting of 63 water molecules and a single solvated ion, with the excess charge compensated by a uniform background charge. The size of the cells was chosen to yield the experimental density of liquid water under ambient conditions. The simulations were carried out using Born–Oppenheimer MD with the Qbox code (45), with the interatomic force derived from DFT and the Perdew, Burke, and Ernzerhof approximation for the exchange-correlation energy functional (46). The interaction between valence electrons and ionic cores was represented by norm-conserving pseudo-potentials (47), and the electronic wave functions were expanded in a plane-wave basis set truncated at a cutoff energy of 85 Ry. All hydrogen atoms were replaced with deuterium to maximize the allowable time step, which was chosen to be 10 atomic units. The equilibration runs were carried out at an elevated temperature of \( T = 400 \) K to recover the experimental water structure and diffusion, while also providing a good description of the ion solvation at room temperature (48). For the analysis of structural properties, the statistics were collected over 45-ps microcanonical simulations after an equilibration run of 15 ps.

On the basis of the simulations, we evaluated the strength of the hydration shell of the anions (E sodom) using cluster calculations. Specifically, E sodom was approximated as the binding energy of the ion-water clusters, \( \chi (\text{H}_2\text{O}_n) \), where \( \chi \) corresponds to the anions and \( n \) is the number of water molecules in the first ion solvation shell. Here, the strength of the ion hydration shell is estimated as \( E_{\text{sodom}} = E(\chi (\text{H}_2\text{O}_n)) - E(\chi (\text{H}_2\text{O}')) - E(\text{H}_2\text{O}_n) \), where \( E(\chi (\text{H}_2\text{O}_n)) \), \( E(\chi (\text{H}_2\text{O}')) \), and \( E(\text{H}_2\text{O}_n) \) are the energies of the \( \chi (\text{H}_2\text{O}_n) \) and \( \chi (\text{H}_2\text{O}') \) clusters and the ion \( \chi \) in vacuum, respectively. The calculation was carried out with a uniform positive background charge to neutralize the system, with Markov–Payne correction to account for spurious interactions between periodic images (49). The final values of E sodom were obtained by averaging the results over 500 configurations of \( \chi (\text{H}_2\text{O}_n) \) clusters extracted directly from the corresponding simulations. For each cluster, the number of water molecules was determined using the distance cutoff as the first minimum of the ion–oxygen radial distribution functions of the ions. This distance cutoff represents the hydrated radius of the ion.

**Property curation and feature selection models**

We collected ionic properties and descriptors from previously published work (table S5), information extracted from ion SMILES strings in the RDKit package (50–52) (table S6), and DFT simulations conducted herein (tables S7 and S8). DFT simulations were performed with a development version of graphics processing unit–accelerated TeraChem v1.9 (53, 54). The B3LYP (55–57) global hybrid functional with semiempirical D3 dispersion correction (58–61) was used with an LANL2DZ (62) effective core potential basis set for heavy atoms (i.e., Br, I, and Mn) and the 6-31G* basis for all other atoms. Relative properties of the ions are expected to be insensitive to this functional/basis set choice. For isolated ion calculations, properties (table S7) were computed in both the gas phase and a dielectric approximating water in bulk (ε = 78) and under confinement (ε = 30) (63) using the conductor-like polarizable continuum model (C-PCM).
solution model (64, 65), as implemented in TeraChem (53, 54). The cluster of the CA unit structure was modeled to study the interaction between ions and the CA (fig. S7). To ensure that we sample equivalent CA effects for each ion, geometry optimizations of ions are carried out with the CA fixed. The initial positions of the ions are only considered over the acetyl groups and the tetrahydropyran rings, which carry the most negative and positive charges, respectively, and are therefore assumed to represent the most and the least favorable binding sites for the anions (fig. S7). Ion-CA interaction properties (table S7) were obtained under two dielectric constant environments to represent interactions in bulk water (ε = 78) and under confinement (ε = 30) (63), similar to the isolated ion calculations.

RFA that adds features sequentially to the target model (66) to eliminate less informative features was used for building the linear regression model for all the properties. The models are judged by leave-one-out cross-validation (LOOCV) (67), and the MAE is used to estimate the model’s performance. Consistent with a typical RFA approach, at each iteration, the linear regression model implemented in scikit-learn (68) is trained with a new feature set, and a descriptor is kept only if adding the new feature yields a decrease in the MAE of >1% (fig. S12). For the selected subset of features, the feature importance is ranked by the absolute coefficient in the linear regression model (table S9). The absolute coefficient determined for each feature is obtained by averaging the absolute coefficients of the 18 linear regression models generated during LOOCV. We also evaluate the L1-regularized, least absolute shrinkage and selection operator linear least-square regression (69) to train the model for feature selection as implemented in scikit-learn (68). The regularization hyperparameter λ was obtained with grid search in the range [1 × 10−8, 1 × 10−4]. The optimized hyperparameters, MAE, and two model’s performance comparison for target properties are compared in table S11.

SUPPLEMENTARY MATERIALS

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REFERENCES AND NOTES

1. P. D’Odorico, K. F. Davis, L. Rosa, J. A. Carr, D. Chiarelli, J. Dell’Angelo, J. Geephart, G. K. MacDonald, D. A. Seekell, S. Suweis, M. C. Rulli, The global food-energy-water nexus. Rev. Geophys. 56, 456–531 (2018).

2. S. K. Patel, C. L. Ritt, A. Deshmukh, Z. Wang, M. Qin, R. Epsztein, M. Elimelech, The relative insignificance of advanced materials in enhancing the energy efficiency of desalination membranes. Proc. Natl. Acad. Sci. U.S.A. 117, 30191–30200 (2020).

3. S. Sahu, M. D’Ventric, M. Zvolak, Dehydration as a universal mechanism for ion selectivity in graphene and other atomically thin pores. Nano Lett. 17, 4719–4724 (2017).

4. R. C. Smith, P. Mukherjee, A. K. SenGupta, Comment on "Experimental energy barriers to transporting anions through nanofiltration membranes". Environ. Sci. Technol. 47, 8985–8986 (2013).

5. R. Epsztein, E. Shaulsky, M. Qin, M. Elimelech, Activation behavior for ion permeation in ion-exchange membranes: Role of ion dehydration in selective transport. J. Membr. Sci. 580, 316–326 (2019).

6. J. Abrahams, K. S. Vassu, C. D. Williams, K. Gopinadhan, Y. Su, C. T. Chen, J. Dix, E. Prestat, S. J. Haigh, J. V. Grigorieva, P. Carbonne, A. K. Geim, R. R. Nair, Tunable sieving of ions using graphene oxide membranes. Nat. Nanotechnol. 12, 546–550 (2017).

7. F. Aydin, M. R. Ceron, S. A. Hawks, D. I. Oyarzun, C. Zhan, T. A. Pham, M. Stadermann, P. G. Campbell, Selectivity of nitrate and chloride ions in microporous carbons: The role of anisotropic hydration and applied potentials. Nanoscale 12, 20292–20299 (2020).

8. F. Aydin, C. Zhan, C. Ritt, R. Epsztein, M. Elimelech, E. Schwiegker, T. A. Pham, Similarities and differences between potassium and ammonium ions in liquid water: A first-principles study. Phys. Chem. Chem. Phys. 22, 2540–2548 (2020).

9. G. Portella, J. S. Hub, M. D. Vesper, B. L. de Groot, Not only enthalpy: Large entropy contribution to ion permeation barriers in single-file channels. Biophys. J. 95, 2275–2282 (2008).

10. M. Neek-Amal, F. M. Peeters, I. V. Grigorieva, A. K. Geim, Commensurability effects in viscosity of nanofrined water. ACS Nano 10, 3685–3692 (2016).

11. L. Fumagalli, A. Esfandiar, R. Fabregas, S. Hu, P. Ares, A. Jamardanan, Q. Yang, B. Radha, T. Taniguchi, K. Watanabe, G. Gorilla, K. S. Novoselov, A. K. Geim, Anomalously low dielectric constant of confined water. Science 360, 1339–1342 (2018).

12. B. J. Zolwinski, H. Eyring, C. E. Reese, Diffusion and membrane permeability. J. Phys. Chem. 53, 1426–1453 (1949).

13. X. Zhou, Z. Wang, R. Epsztein, C. Zhan, W. Li, D. Fortner John, A. Pham Tuan, J.-H. Kim, M. Elimelech, Intrapore energy barriers govern ion transport and selectivity of desalination membranes. Sci. Adv. 6, eab90450 (2020).

14. U. Ryde, A fundamental view of enthalpy-entropy compensation. Medchemcomm 5, 1324–1336 (2014).

15. J. D. Chodera, D. L. Mobley, Entropy-enthalpy compensation: Role and ramifications in biomolecular ligand recognition and design. Annu. Rev. Biophys. 42, 121–142 (2013).

16. G. Landrum, Rdkit: Open-source cheminformatics (2006); www.rdkit.org [accessed 1 December 2020].

17. A. Nandy, J. Zhu, J. P. Janet, C. Duan, R. B. Getman, H. J. Kulik, Machine learning accelerates the discovery of design rules and exceptions in stable metal–oxo intermediate formation. ACS Catal. 9, 8243–8255 (2019).

18. S. M. Mosavi, A. Nandy, K. M. Jablonka, D. Ongari, J. F. Janet, P. G. Boyd, Y. Lee, B. Smit, H. J. Kulik, Understanding the diversity of the metal-organic framework ecosystem. Nat. Commun. 11, 4068 (2020).

19. S. J. Grabowski, Hydrogen bonds with BF₄⁻ anion as a proton acceptor. Crystals 10, 460 (2020).

20. C. D. Wick, I. F. W. Kuo, C. J. Mundy, L. X. Dang, The effect of polarizability for understanding the molecular structure of aqueous interfaces. J. Chem. Theory Comput. 3, 2002–2010 (2007).

21. R. Lunney, S. Rajender, Enthalpy–entropy compensation phenomena in water solutions of proteins and small molecules: A ubiquitous property of water. Biopolymers 9, 1125–1227 (1970).
Machine learning reveals key ion selectivity mechanisms in polymeric membranes with subnanometer pores
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