Higher-twist contributions to the transverse momentum broadening in semi-inclusive deep inelastic scattering off large nuclei

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Multiple scattering leads to transverse momentum broadening of the struck quark in semi-inclusive deeply inelastic scatterings (SIDIS). Nuclear broadening of the transverse momentum squared at the leading twist is determined by the twist-four collinear quark-gluon correlation function of the target nucleus that is in turn related to the jet transport parameter inside the nuclear medium. The twist-six contributions to the transverse momentum broadening are calculated as power corrections \( \sim 1/Q^2 \). Such power corrections are found to have no extra nuclear enhancement beyond the twist-four matrix elements and are determined by the nuclear modification of collinear parton distribution and correlation functions. They become important for an accurate extraction of the jet transport parameter inside large nuclei and its scale evolution at intermediate values of the hard scale \( Q^2 \).

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I. INTRODUCTION

Multiple scattering of a propagating parton inside a medium leads to many interesting phenomena such as transverse momentum broadening and parton energy loss [1,2]. These phenomena as observed in experiments in both high-energy heavy-ion collisions and semi-inclusive deeply inelastic scatterings (SIDIS) can in turn be used to extract properties of hot and cold nuclear matter. One of these medium properties as probed by propagating partons is the jet transport parameter \( \hat{q} \). It is defined as the transverse momentum broadening squared per unit length \( \hat{q}^2 / \langle \hat{q}^2 \rangle \) and measures the interaction strength between the energetic parton and the medium. A recent comprehensive phenomenological study [7] of experimental data on jet quenching in high-energy heavy-ion collisions at both the Relativistic Heavy-ion Collider (RHIC) and the Large Hadron Collider (LHC) has extracted values of the jet transport parameter at the center of the produced dense matter. They are about two orders of magnitude higher than that in a cold nucleus as extracted from experimental data on semi-inclusive deeply inelastic scatterings (SIDIS). Nuclear broadening of the transverse momentum squared at the leading twist is determined by the twist-four collinear quark-gluon correlation function of the target nucleus that is in turn related to the jet transport parameter inside the nuclear medium. The accuracy of the determination of the jet transport parameter from experimental data on transverse momentum broadening and its scale evolution should be important for a more accurate determination of the jet transport parameter inside large nuclei and its scale evolution at intermediate values of the hard scale \( Q^2 \).

Multiple soft interactions between the struck quark and the remnant nucleus in SIDIS can also be resummed in the eikonal limit into the gauge link in the transverse momentum dependent (TMD) parton distribution functions [20]. The transverse momentum broadening in a large nucleus arises naturally from the expectation value of the gauge link between the nuclear state. Under a maximal two-gluon correlation approximation, the transverse momentum broadening takes the form of a Gaussian distribution with the width given by the path-integrated jet transport parameter [21]. Within a systematic collinear expansion of the hard parts of partonic scattering, one can express the cross section of SIDIS in terms of TMD parton distribution and correlation functions with different power corrections [22]. Calculations of the SIDIS cross section have been carried out in the leading order and up to twist-4 power corrections [22]. The results have been applied to the study of nuclear dependence of the azimuth asymmetry in both unpolarized [24] and polarized nuclear targets [25,26]. We will employ these cross sections in this paper to study the transverse momentum broadening up to \( O(1/Q^2) \) corrections.

The remainder of this paper is organized as the following. In Section III we present the kinematics of SIDIS and review the differential cross section of the SIDIS process in terms of the TMD parton distribution and correlation functions within the collinear expansion.
In Section [II] we calculate the transverse momentum squared ($k_\perp^2$) weighted differential SIDIS cross section. The corresponding $k_\perp^2$-weighted parton distribution and correlation functions are shown to become higher-twist collinear (transverse momentum integrated) matrix elements which can be related to the jet transport parameter. We calculate the transverse momentum broadening up to $O(1/Q^2)$ corrections in Section [V]. Conclusions and outlooks are given in Section [V].

II. SIDIS CROSS SECTION UP TO $O(1/Q^2)$

We consider the differential cross section of the SIDIS process $e^{-}(\ell) + A(p) \rightarrow e^{-}(\ell') + q(k) + X(p_X)$ with an unpolarized electron beam $e^{-}$ and an unpolarized target nucleus $A$ which carries momentum $p$ per nucleon in the infinite momentum frame,

$$d\sigma = \frac{(4\pi\alpha_{em})^2}{2sQ^4} \frac{d^3\ell'}{2E_{\ell'}(2\pi)^3} dW^{\mu\nu} L_{\mu\nu},$$ (1)

where $\alpha_{em}$ is the fine structure constant in QED, $s$ is the Mandelstam variable for the center-of-mass energy squared, $q = \ell - \ell'$ and $Q^2 = -q^2$ is the virtuality of the virtual photon that probes the nucleus. We neglect all the masses of particles.

The leptonic tensor $L^{\mu\nu}$ and hadronic tensor $W^{\mu\nu}$ are defined as,

$$L_{\mu\nu} = \text{Tr}[f_{\gamma \mu} f_{\gamma \nu}] = 4(\epsilon_{\mu} \epsilon_{\nu} + \epsilon_{\mu} \epsilon_{\nu}' - \ell \cdot \epsilon' g_{\mu\nu}),$$ (2)

$$W^{\mu\nu} = \frac{1}{2\pi} \sum_{X} (A|J_{\mu}(0)|X + q)(X + q|J_{\nu}(0)|A) \times (2\pi)^4 \delta^4(p + q - k - p_X),$$ (3)

respectively. In the infinite momentum frame, we parameterize the momenta in the following conventional light-cone expansion [22, 23],

$$p^\mu = p^+ \hat{n}^\mu,$$ (4)

$$\ell^\mu = \frac{1 - y}{y} x_B p^+ \hat{n}^\mu + \frac{1}{y} q^- n^\mu + \ell_T^\mu,$$ (5)

$$\ell'^\mu = \frac{1}{y} x_B p^+ \hat{n}^\mu + \frac{1 - y}{y} q^- n^\mu + \ell'^T^\mu,$$ (6)

$$q^\mu = - x_B p^+ \hat{n}^\mu + q^- n^\mu,$$ (7)

where the unit vectors are taken as $\hat{n}^\mu = (1, 0, 0, 0), n^\mu = (0, 1, 0, 0)$.

At the leading order (LO) of a perturbative expansion of the hard photon-parton scattering processes, one still has to consider multiple interaction between the struck quark and the remanent nucleus through soft gluon exchanges as shown in Fig. [II]. The hadronic tensor can be written as a sum of the contributions from all possible diagrams with multiple gluon exchanges. With collinear expansion of the hard partonic parts, the hadronic tensor can be reorganized as products of collinear hard parts and gauge invariant TMD quark (gluon) correlation functions [15, 22, 27–30]. One can further reorganize the final differential cross section in terms of a power expansion in $1/Q$. The differential cross section of the unpolarized SIDIS process $e^{-}(\ell) + A(p) \rightarrow e^{-}(\ell') + q(k) + X(p_X)$ up to the power of $O(1/Q^2)$ takes the form [22],

\[
\frac{d\sigma^A}{dx_B dy d^2k_\perp} = \frac{2\pi\alpha_{em}^2 q^2}{Q^2 y} \left\{ 1 + (1 - y)^2 \left[ f_{q}^{A}(x_B, k_\perp) - 4(2 - y) \sqrt{1 - y} \frac{\vec{k}_\perp}{Q} \cdot \vec{k}_\perp \cdot f_{q}^{A}(x_B, \vec{k}_\perp) \cos \phi \right. \right.
\]

\[
\left. -4(1 - y) \frac{|\vec{k}_\perp|^2}{Q^2} x_B [\varphi_{1/2}^{(1)A}(x_B, k_\perp) - \varphi_{1/2}^{(1)A}(x_B, \vec{k}_\perp)] \cos 2\phi + 16(1 - y) \frac{x_B^2 M^2}{Q^2} f_{q_{(-)}^{A}}(x_B, \vec{k}_\perp) \right) \left. -2 \left[ 1 + (1 - y)^2 \right] \frac{|\vec{k}_\perp|^2}{Q^2} x_B \left[ \varphi_{2}^{(2)A}(x_B, k_\perp) - \varphi_{2}^{(2)A}(x_B, \vec{k}_\perp) \right] \right\},
\]

(8)

where the TMD parton distribution and correlation functions $f_{q}^{A}$, $f_{q_{(-)}^{A}}, \varphi_{1/2}^{(1)A}, \varphi_{1/2}^{(2)A}, \varphi_{2}^{(2)A}$ and $\varphi_{2}^{(2)A}$ in
terms of matrix elements can be found in Eqs. (A2)–(A13) in the appendix. The above expansion in terms of TMD parton distribution and correlation functions is a generalized expansion similar to the collinear twist expansion. The first term is the leading twist contribution proportional to the TMD quark distribution function $f_q^A(x_B, k_{||})$. This gives rise to the normal collinear quark distribution function after integration over the transverse momentum. The second term is the twist-3 contribution with an azimuthal asymmetry $\cos \phi$. The rest are twist-four contributions. All high-twist contributions are suppressed by $O([k_{||}/Q]^n, [M/Q]^n)$.

III. NUCLEAR DEPENDENCE OF HIGHER-TWIST MATRIX ELEMENTS

To study the transverse momentum broadening, we need to calculate the $k_{||}$-weight-integrated differential cross section. Multiplying with $k_{||}$ and integrating over the transverse momentum, one obtains from Eq. (9),

$$\frac{d\langle \vec{k}_{||}^2 f_q^A \rangle}{dxdy} = \frac{2\pi^2 e^2}{Q^2} \left\{ \left[ 1 + (1 - y)^2 \right] \langle \vec{k}_{||}^2 f_q^A \rangle(x_B) \right. \\
+ 16(1 - y)x_B^2 M^2 \langle \vec{k}_{||}^2 f_q^A \rangle(x_B) \\
- 2[1 + (1 - y)^2]x_B \\
\times \left[ \langle \vec{k}_{||}^2 \phi_{||}^{(2)A} \rangle(x_B) - \langle \vec{k}_{||}^2 \phi_{||}^{(2)A} \rangle(x_B) \right] \right\},$$

where $\langle \vec{k}_{||}^2 f_q^A \rangle(x_B)$, $\langle \vec{k}_{||}^2 f_q^A \rangle(x_B)$, $\langle \vec{k}_{||}^2 \phi_{||}^{(2)A} \rangle(x_B)$ and $\langle \vec{k}_{||}^2 \phi_{||}^{(2)A} \rangle(x_B)$ are $k_{||}$-weight-integrated parton distributions/correlation functions of $f_q^A(x_B, k_{||})$, $f_q^A(x_B, k_{||})$, $\phi_{||}^{(2)A}(x_B, k_{||})$ and $\phi_{||}^{(2)A}(x_B, k_{||})$, respectively [see Eqs. (A14)–(A19) in the appendix]. These $k_{||}$-weight-integrated parton distribution and correlation functions contain $k_{||}$-weighted matrix elements. Through partial integration in the transverse momentum $k_{||}$, one can convert each $k_{||}$ into a partial derivative with respect to the transverse coordinate. The field operators in $k_{||}$-weight-integrated parton distribution and correlation functions are always two twist higher than those in the corresponding distribution and correlation functions without $k_{||}$-weight. Therefore the above $k_{||}$-weighted cross section should contain parton correlation functions up to twist-six.

Take the first term in Eq. (9) as an example, the $k_{||}$-weight-integrated parton distribution function,

$$\langle \vec{k}_{||}^2 f_q^A \rangle(x) \equiv \int \vec{k}_{||}^2 f_q^A(x, \vec{k}_{||}) \vec{k}_{||}^2 \\
= - \int dydy' \frac{d^2k_{||}^2}{(2\pi)^3} e^{ixp^+yp^-} e^{-ixp^+yp^-} \langle \vec{F}_{||}^+q(y') F_{||}^+q(\vec{r}_{||})\rangle \langle \vec{F}_{||}^+q(y') \rangle \langle \vec{F}_{||}^+q(\vec{r}_{||})\rangle,$$

is in fact a twist-four two-parton correlation function. In the above equation, we have used the identity [21],

$$-i\partial^\mu \mathcal{L}(\infty; y^-, \vec{y}_{||}) = \mathcal{L}(\infty; y^-, \vec{y}_{||}) \left[ D^\mu_{||}(y) + g \int_{y'}^\infty d\xi^- \mathcal{L}(y'; \xi^-, \vec{y}_{||}) F^\mu_{||}(\xi^-, \vec{y}_{||}) \mathcal{L}(\xi^-; y^-, \vec{y}_{||}) \right],$$

for a derivative acting on a gauge link,

$$\mathcal{L}(z^-; y^-, \vec{y}_{||}) = \mathcal{P} \exp \left[ -ig \int_{y'}^{z^-} d\xi^- A^+(\xi^-, \vec{y}_{||}) \right].$$

The covariant derivative is defined as $D^\mu_{||}(y) = -i\partial^\mu_{||} + gA^\mu_{||}(y)$. Note that the gauge link in Eq. (11) between two space-time points with a transverse displacement is defined as,

$$\mathcal{L}(0; y) = \mathcal{L}^I(\infty; 0) \mathcal{L}(\infty; y^-, \vec{y}_{||}),$$

in a covariant gauge. According to the above identity, the double derivatives on the gauge link in Eq. (11) produce three different contributions. We only keep the term with two gluon field strength operators which is enhanced by the nuclear size with a factor of $A^{1/3}$ due to the double path integrations across the nuclear size. Other terms that have one or two covariant derivatives on the quark field are ignored because they do not have such a nuclear enhancement. We also omit the gauge link in the final expression of the parton correlation function for brevity. Note that one can change the limits of the integration over $\eta^-$ to the same as $\xi^-$ in Eq. (11) with an overall factor of 1/2.

Assuming a large and loosely bound nucleus, one can factorize the twist-four quark-gluon correlation function as a product of the quark distribution function for A

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nucleons and soft gluon distribution density integrated over the size of the nucleus \[\text{[31]},\]

\[
\langle A|\bar{\psi}(0)\gamma^+F^+_{\perp}(\eta^{-})F^+_{\perp}(\xi^{-})\psi(y^{-})|A\rangle
\approx A(N)\langle\bar{\psi}(0)\gamma^+\psi(y^{-})|N\rangle\frac{1}{2N_c}\frac{\rho_N(\xi^{-})}{2p^-}
\times \langle N|F^+_{\perp}(\xi^{-} - \frac{\lambda^-}{2})F^+_{\perp}(\xi^{-} + \frac{\lambda^-}{2})|N\rangle,
\]

where \(\xi_N = (\eta^{-} + \xi^{-})/2\) and \(\lambda^- = \xi^{-} - \eta^{-}\). We have taken the medium ensemble average,

\[
\int \frac{d^3p}{(2\pi)^32p^+}f_A(p,\xi_N)(N)\cdots|N\rangle = \frac{\rho^A_N(\xi_N)}{2p^+}(N)\cdots|N\rangle,
\]

for the gluon field strengths over all possible nucleons inside the nucleus and \(\rho^A_N(\xi_N)\) is the spatial nucleon density normalized to the atomic number \(A\). Given the definition of the collinear quark and gluon distribution functions,

\[
f_q^N(x) = \int \frac{dy^-}{2\pi}e^{ixp^+y^-}\langle N|\bar{\psi}(0)\gamma^+\psi(y^-)|N\rangle,
\]

\[
xg_N(x) = -\int \frac{d\lambda^-}{2\pi p^+}e^{ixp^+\lambda^-}\langle N|F^+_{\perp}(0)F^+_{\perp}(\lambda^-)|N\rangle,
\]

the \(\vec{k}_1^4\)-weight-integrated quark distribution function becomes

\[
\langle \vec{k}_1^4 f_q^A(x) \rangle(x) = A f_q^N(x) \int d\xi_N \bar{q}_F(\xi_N) + \mathcal{O}(A),
\]

where

\[
\bar{q}_F(\xi_N) = \frac{2\pi^2\alpha_s}{N_c} \rho^A_N(\xi_N) [x_gg_N(x_g)]_{x_g=0}.
\]

is the jet transport parameter for a quark. It represents the transverse momentum broadening squared per unit length. The averaged total transverse momentum broadening squared inside a nucleus is then,

\[
\Delta_2 F = \int d\xi_N \bar{q}_F(\xi_N),
\]

which should be proportional to the nuclear size \(R_A \approx 1.12A^{1/3}\) fm.

One can obtain similar relation for the \(\vec{k}_1^4\)-weight-integrated parton distribution function in the second term of Eq. \[\text{[19]},\]

\[
\langle \vec{k}_1^4 f_q^A(-\xi_N) \rangle(x) = A f_q^N(x) \Delta_2 F + \mathcal{O}(A),
\]

where

\[
f^{A}_{q(-\xi_N)}(x,\vec{k}_\perp) = \frac{p^+}{M^2} \int \frac{dy^-}{2\pi} e^{ixp^+y^-} \langle A|\bar{\psi}(0)\frac{p^+}{2}\psi(y^-)|A\rangle,
\]

is a twist-4 collinear quark distribution function.

Since the integration over the length of the nucleus should be proportional to the nuclear size \(R_A \sim A^{1/3}\), the nuclear enhanced parts of both \(\langle \vec{k}_1^4 f_q^A(x) \rangle\) and \(\langle \vec{k}_1^4 f_{q(-\xi_N)}^A(x) \rangle\) are proportional to \(A^{4/3}\). One can neglect other contributions that are not enhanced by the nuclear size, including those that describe quark-gluon correlation functions inside a single nucleon.

The third term of Eq. \[\text{[19]},\] contains contributions from double scattering processes in Fig. \[\text{[1]},\] with two gluon exchanges. The associated parton correlation functions have two covariant derivatives and have contributions from both left and right-cut diagrams,

\[
\varphi_{(2)}^{(2)}(x,\vec{k}_\perp) = \frac{1}{2} \left[ \varphi_{(2,L)}^{(2)}(x,\vec{k}_\perp) + \varphi_{(2,R)}^{(2)}(x,\vec{k}_\perp) \right].
\]

The corresponding \(\vec{k}_1^4\)-weight-integrated parton correlation functions can be similarly simplified assuming factorization in a large and loosely bound nucleus,
\[
\langle \vec{k}_1^4 \varphi_{(2,L)}^A \rangle (x) = \int \frac{dy^-d^2y_\perp d^2\vec{k}_1^+ dz^-}{(2\pi)^3} i\theta(z^-)e^{ixp^+y^- - i\vec{k}_1^+ \cdot \vec{y}} \vec{k}_1^2
\]
\[
\times \langle A| \bar{\psi}(0) \gamma^+ \mathcal{L}(0; z^-) D_{1\sigma}(z^-, 0_\perp) D_{1\rho}^\sigma(z^-, 0_\perp) \mathcal{L}(z^-; 0_\perp; y) \psi(y)|A \rangle
\]
\[
\simeq - \int \frac{dy^-d^2y_\perp d^2\vec{k}_1^+ dz^-}{2\pi} i\theta(z^-)e^{ixp^+y^-} \int_{y^-}^{\infty} d\xi^- \int_{\xi^-}^{\infty} d\eta^- 2g^2
\]
\[
\times \langle A| \bar{\psi}(0) \gamma^+ \mathcal{L}(z^-; 0_\perp) D_{1\rho}(z^-, 0_\perp) D_{1\sigma}(z^-; 0_\perp) \mathcal{L}(z^-; 0_\perp; y) \psi(y)|A \rangle,
\]
where we again omit the gauge links in the final expression for brevity. Using Eq. (11) we can also get,
\[
\langle \vec{k}_1^4 \varphi_{(2,R)}^A \rangle (x) = \int \frac{dy^-d^2y_\perp d^2\vec{k}_1^+ dz^-}{(2\pi)^3} i\theta(z^- - y^-)e^{ixp^+y^-} \int_0^{\infty} d\xi^- \int_{\xi^-}^{\infty} d\eta^- 2g^2
\]
\[
\times \langle A| \bar{\psi}(0) \gamma^+ F_{1\rho}^p (\xi^-; 0_\perp) F_{1\sigma}^p (\eta^-; 0_\perp) D_{1\sigma}(z^-; 0_\perp) D_{1\rho}^\sigma(z^-; 0_\perp) \mathcal{L}(z^-; 0_\perp; y) \psi(y)|A \rangle,
\]
which help to reduce the \( \vec{k}_1^4 \)-weight-integrated parton correlation functions to the following forms,
\[
\langle \vec{k}_1^4 \varphi_{(2,L)}^A \rangle (x) \simeq \int \frac{dy^-d^2y_\perp d^2\vec{k}_1^+ dz^-}{2\pi} i\theta(z^-)e^{ixp^+y^-} \int_{y^-}^{\infty} d\xi^- \int_{\xi^-}^{\infty} d\eta^- \int_{\xi^-}^{\infty} d\xi^- \int_{\xi^-}^{\infty} d\eta^- 2g^2
\]
\[
\times (-4g^2) \langle A| \bar{\psi}(0) \gamma^+ F_{1\rho}^p (\xi^-) F_{1\sigma}^p (\eta^-) F_{1\rho}^p (\xi^-) \mathcal{L}(z^-; 0_\perp; y) \psi(y)|A \rangle,
\]
\[
\langle \vec{k}_1^4 \varphi_{(2,R)}^A \rangle (x) \simeq \int \frac{dy^-d^2y_\perp d^2\vec{k}_1^+ dz^-}{2\pi} i\theta(z^- - y^-)e^{ixp^+y^-} \int_0^{\infty} d\xi^- \int_{\xi^-}^{\infty} d\eta^- \int_{\xi^-}^{\infty} d\eta^- 2g^2
\]
\[
\times 4g^4 \langle A| \bar{\psi}(0) \gamma^+ F_{1\rho}^p (\xi^-) F_{1\sigma}^p (\eta^-) F_{1\rho}^p (\xi^-) \mathcal{L}(z^-; 0_\perp; y) \psi(y)|A \rangle
\]
These are twist-six matrix elements for parton correlation functions inside a nucleus. Under the same approximation of a large and loosely bound nucleus, one can similarly factorize these twist-six matrix elements into products of twist-four or twist-two matrix elements in a general form,
\[
\langle \vec{k}_1^4 \varphi_{(2,L/R)}^A \rangle (x) \simeq A^{5/3}(\bar{\psi}\psi)_N \otimes (FF)_N \otimes (FF)_N
\]
\[
+ A^{4/3}(\bar{\psi}FF\psi)_N \otimes (FF)_N
\]
\[
+ A^{4/3}(FFF\psi)_N \otimes (\bar{\psi}\psi)_N + O(A),
\]
where \( \langle \ldots \rangle_N \) represents the expectation value over a nucleon state. Since the hard photon-quark scattering can happen in any nucleon in the nucleus, summation of these interactions over all nucleons inside the nucleus contributes to a factor \( A \). Integration over the position of another nucleon in the secondary interaction along the propagation path of the struck quark will give another factor of \( R_A \sim A^{1/3} \). These matrix elements are enhanced by a factor of \( A^{1/3} \) for each additional nucleons involved in the interaction beside the hard photon-quark scattering. Other contributions without the nuclear en-
hancement can be neglected here. Let us examine separately contributions from the left and right-cut diagrams in the first term in Eq. (29) with the most nuclear enhancement,

\begin{align}
\langle \bar{K}_1^4 \varphi_{1,\perp}^{(2,L)A}\rangle_1(x) &\approx -A \int \frac{dy^-}{2\pi} e^{ip^+y^-} \langle N|\bar{\psi}(0)\gamma^+\frac{1}{2}\psi(y^-)|N\rangle \int_0^\infty d\xi^- \int_{\xi^-}^\infty d\eta^- 2g^2\langle N|F_{\perp\rho}^+(\xi^-)F_{\perp\rho}^+(\eta^-)|N\rangle \frac{\rho_A^N(\xi^-) \rho_A^N(\xi^-_N)}{2p^-} \\
&\times \int p^+dz^-i\theta(z^-) \int_{\xi^-}^{\xi^-_N} d\xi'' \int_{\xi''}^{\xi''_N} d\eta'' 2g^2\langle N|F_{\perp\rho}^+(\xi'')F_{\perp\rho}^+(\eta'')|N\rangle \frac{\rho_A^N(\xi''_N) \rho_A^N(\xi''_N)}{2p^-} \\
&= A \int \frac{dy^-}{2\pi} e^{ip^+y^-} \langle N|\bar{\psi}(0)\gamma^+\frac{1}{2}\psi(y^-)|N\rangle \int_0^\infty d\xi^- \int_{\xi^-}^\infty d\eta^- 2g^2\langle N|F_{\perp\rho}^+(\xi^-)F_{\perp\rho}^+(\eta^-)|N\rangle \frac{\rho_A^N(\xi^-) \rho_A^N(\xi^-_N)}{2p^-} \\
&\times \int p^+dz^-i\theta(z^-) \int_{\xi^-}^{\xi^-_N} d\xi'' \int_{\xi''}^{\xi''_N} d\eta'' 2g^2\langle N|F_{\perp\rho}^+(\xi'')F_{\perp\rho}^+(\eta'')|N\rangle \frac{\rho_A^N(\xi''_N) \rho_A^N(\xi''_N)}{2p^-},
\end{align}

where \(\xi^-_N = (\eta^- + \xi^-)/2\) and \(\xi''^-_N = (\eta''^- + \xi''^-)/2\) are the light-cone positions of the nucleons. In Eq. (30) we approximate the integral boundary for \(\xi^- \in (y^-, \infty)\) by \(\xi^- \in (0, \infty)\). Since \(y^-\) is confined to the size of a nucleon for large and moderate values of momentum fraction \(x\), the difference should be small. In Eq. (31) we first interchange the integration variables \(\eta''^- \leftrightarrow \xi''^-\) and then make variable changes \(\xi''^- \to \xi''^- - y^-\) and \(\eta''^- \to \eta''^- - y^-\). We also assume the translational invariance of the matrix element \(\langle N|F_{\perp\rho}^+(\xi''^- + y^-)F_{\perp\rho}^+(\eta''^- + y^-)|N\rangle = \langle N|F_{\perp\rho}^+(\xi''^-)F_{\perp\rho}^+(\eta''^-)|N\rangle\) and \(\rho_A^N(\xi''^- + y^-) \approx \rho_A^N(\xi''^-)\). The final result in Eq. (31) is obtained with another variable change \(z^- \to z^- - y^-\).

Note that there is a sign difference between contributions from the left and right-cut diagrams. The net sum of these two contributions gives,

\begin{align}
\langle \bar{K}_1^4 \varphi_{1,\perp}^{(2)A}\rangle_1(x) &= \frac{1}{2} \left[ \langle \bar{K}_1^4 \varphi_{1,\perp}^{(2,L)A}\rangle_1(x) + \langle \bar{K}_1^4 \varphi_{1,\perp}^{(2,R)A}\rangle_1(x) \right] \\
&\approx Af_q^N(x) \Delta_{2F} \int p^+dz^-i\theta(z^-) \int_{\xi^-}^{\xi^-_N} d\xi'' \int_{\xi''}^{\xi''_N} d\eta'' 2g^2\langle N|F_{\perp\rho}^+(\xi'')F_{\perp\rho}^+(\eta'')|N\rangle \frac{\rho_A^N(\xi''_N) \rho_A^N(\xi''_N)}{2p^-} = 0,
\end{align}

that contains a commutator of the gluon field strength tensor which should vanish on the light-cone \(\xi^- \in (0, \infty)\). Therefore, \(\langle \bar{K}_1^4 \varphi_{1,\perp}^{(2)A}\rangle_1(x)\) has no leading contribution with \(A^{5/3}\) nuclear enhancement due to the cancellation between left and right-cut diagrams.

Using similar techniques one finds that the contributions from the third term of Eq. (29) also vanishes due to cancellation between left and right-cut diagrams. The only remaining contribution with nuclear enhancement is the second term in Eq. (29) which can be cast in the form,

\begin{align}
\langle \bar{K}_1^4 \varphi_{1,\perp}^{(2)A}\rangle_1(x) = Af_q^N(x) \Delta_{2F} + O(A),
\end{align}

where
\[
\psi_{\perp}^{(2,L)N}(x) = \int \frac{dy^-}{2\pi} \frac{d\vec{p}^+}{2\pi} e^{i\vec{p}^+ \cdot \vec{y}^-} i\theta(z^-) \langle N|\bar{\psi}(0)\gamma^+ D_{\perp}^2(z^-)\psi(y^-)|N \rangle
\] (34)

\[
\psi_{\perp}^{(2,R)N}(x) = \int \frac{dy^-}{2\pi} \frac{d\vec{p}^+}{2\pi} e^{i\vec{p}^+ \cdot \vec{y}^-} (-i)\theta(z^- - y^-) \langle N|\bar{\psi}(0)\gamma^+ D_{\perp}^2(z^-)\psi(y^-)|N \rangle,
\] (35)

\[
\psi_{\perp}^{(2)N}(x) = \frac{1}{2} \left[ \psi_{\perp}^{(2,L)N}(x) + \psi_{\perp}^{(2,R)N}(x) \right] = i\vec{p}^+ \int \frac{dy^-}{4\pi} \int_0^y \frac{d\vec{p}^+ e^{i\vec{p}^+ \cdot \vec{y}^-} \langle N|\bar{\psi}(0)\gamma^+ D_{\perp}^2(z^-)\psi(y^-)|N \rangle. \] (36)

are twist-four parton correlation functions for a nucleon state. We have omitted the gauge links in the above expressions for brevity. One can similarly find that

\[
\langle \tilde{k}_1^2 \varphi_{\perp}^{(2)A}(x) \rangle = A_2F \psi_{\perp}^{(2)N}(x) \Delta_{2F} + O(A). \] (37)

The definition of \( \tilde{\psi}_{\perp}^{(2)N}(x) \) is similar to \( \psi_{\perp}^{(2)N}(x) \). Both are given in the appendix.

**IV. TRANSVERSE MOMENTUM BROADENING**

In the previous section, the \( \tilde{k}_1^2 \)-weighted cross section should also contain contributions that are not enhanced by the nuclear size, including those that contain parton correlations inside a single nucleon. These contributions are essentially the same cross section for a single nucleon target multiplied by the atomic number \( A \). We should subtract these contributions to obtain the final result for the nuclear enhanced \( k_1^2 \)-weighted differential cross section,

\[
\frac{d\tilde{k}_1^2 \sigma^A}{dxdy} - A \frac{d\tilde{k}_1^2 \sigma^N}{dxdy} \approx \frac{2\pi\alpha^2_{em} e^2}{Q^2} A_2F \left\{ [1 + (1 - y)^2] f_q^N(x_B) - 2[1 + (1 - y)^2] x_B \right\} + 16(1 - y) x_B^2 M^2 f_{q^-(x_B)}.
\] (38)

The averaged transverse momentum broadening is defined as,

\[
\Delta \langle p_{\perp}^2 \rangle \equiv \frac{d\tilde{k}_1^2 \sigma^A}{d\sigma^A} - \frac{d\tilde{k}_1^2 \sigma^N}{d\sigma^N},
\] (39)

where the transverse momentum integrated cross section can be obtained from Eq. [3].

\[
\frac{d\sigma^A}{dx_B dy} = \frac{2\pi\alpha^2_{em} e^2}{Q^2} \left\{ [1 + (1 - y)^2] f_q^A(x_B) - 2 [1 + (1 - y)^2] x_B \right\} + 16(1 - y) x_B^2 M^2 f_{q^-(x_B)}.
\] (40)

The above expression for transverse-momentum-integrated cross section is suitable for both nuclear and nucleon targets. The definition of twist-four parton correlation functions \( \tilde{\psi}_{\perp}^{(2)A}(x_B) \) and \( \tilde{\psi}_{\perp}^{(2)A}(x_B) \) (see the appendix) are also suitable for both nuclei and nucleons. Because of the cancellation between contributions from right and left-cut diagrams, the interaction with the soft gluon field is limited within the size of a single nucleon [the integration over \( z^- \) in Eq. [3] for \( \tilde{\psi}_{\perp}^{(2)A}(x_B) \) is limited to the size \( y^- \) of the nucleon, for example].

Therefore, \( \tilde{\psi}_{\perp}^{(2)A}(x_B) \) and \( \tilde{\psi}_{\perp}^{(2)A}(x_B) \) have no nuclear enhancement, similarly as \( f_q^A(x_B) \) and \( f_{q^-(x_B)} \).

Including only the leading nuclear enhancement in the \( \tilde{k}_1^2 \)-weighted and \( \tilde{k}_1^2 \)-integrated differential cross sections and expanding both in terms of power-corrections, one has

\[
\Delta \langle p_{\perp}^2 \rangle \simeq \Delta_{2F} \left\{ \frac{A f_{q^N}(x_B)}{f_q(x_B)} \right\} \left\{ 1 + \frac{16(1 - y)}{[1 + (1 - y)^2] x_B^2 M^2} \right\} + \frac{2 x_B}{Q^2} \left\{ \frac{\tilde{\psi}_{\perp}^{(2)N}(x_B)}{f_q^N(x_B)} - \frac{\tilde{\psi}_{\perp}^{(2)A}(x_B)}{f_q^A(x_B)} \right\} + \frac{\tilde{\psi}_{\perp}^{(2)A}(x_B)}{f_q(x_B)}.
\] (41)

Since all the collinear nuclear parton distribution and correlation functions, \( f_q^A(x_B) \), \( f_{q^-(x_B)} \), \( \tilde{\psi}_{\perp}^{(2)A}(x_B) \) and \( \tilde{\psi}_{\perp}^{(2)A}(x_B) \), have no extra nuclear enhancement beside their linear dependence on \( A \), their
ratios \( f_{qL}^A(xB)/f_{qR}^A(xB), \psi_{1A}^{(2)}(xB)/f_{q}^A(xB) \) and \( \psi_{1A}^{(2)}(xB)/f_{q}^A(xB), \) also do not have any nuclear enhancement. Therefore, the power corrections in the above transverse momentum broadening are not enhanced by the nuclear size. The finite power corrections to the transverse momentum broadening depend, however, on the difference between the collinear parton distribution and correlation functions in a nucleus and that in a free nucleon. If the nuclear parton distribution and correlation functions are just the sums of those of free nucleons, i.e., \( f_{qL}^A(xB) = A f_{qN}^N(xB), \)
\( f_{qR}^A(xB) = A f_{qN}^N(xB), \)
\( \psi_{1A}^{(2)}(xB) = A \psi_{1N}^{(2)N}(xB), \)
\( \psi_{1A}^{(2)}(xB) = A \psi_{1N}^{(2)N}(xB), \) the above power corrections will all vanish. Therefore, the power corrections to the transverse momentum broadening are sensitive to the nuclear modifications of the collinear parton distribution and correlation functions.

V. CONCLUSION

In conclusion, we use the differential TMD cross section of SIDIS up to twist-four contributions to calculate the transverse momentum broadening of the struck quark up to the first power corrections in \( 1/Q^2 \). The \( \vec{k}_T^2 \)-weighted differential cross section depends on higher-twist collinear matrix elements of nuclear states up to twist-six which are shown to factorize approximately into products of jet transport parameter and collinear parton distribution and correlation functions. Because of the cancellation between left and right cut diagrams, these higher-twist matrix elements are shown to have no extra nuclear enhancement in addition to that involved with the jet transport parameter. The final transverse momentum broadening of the struck quark is shown to be proportional to the leading twist result given by a path-integral of the jet transport parameter. The next power corrections are found to have no additional nuclear enhancement. The coefficients of these power corrections are determined by the nuclear modification of the collinear parton distribution and correlation functions.

Such power corrections to the transverse momentum broadening might be important for extracting the jet transport parameter from experimental data. Understanding of these power corrections is also important to the study of the scale evolution of the jet transport parameter according to the QCD evolution equation from the NLO higher-twist contributions to the SIDIS cross section \([10]\), especially at intermediate values of \( Q^2 \).

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Appendix A: Definitions of the matrix elements

The TMD parton distribution and correlation functions in terms of matrix elements of parton field operators that we use in the differential cross sections of SIDIS in Eq. \([8]\) are defined as follows \([23]\),

\[
f_q^A(x, \vec{k}_T) = \int \frac{dy^- d^2 y_\perp}{(2\pi)^3} e^{ixp^+ y^- - i\vec{k}_T \cdot \vec{y}_\perp} \langle A| \bar{\psi}(0) \gamma^+ \mathcal{L}(0; y) \psi(y)|A\rangle, \tag{A1}
\]

\[
f_{q\perp}^A(x, \vec{k}_T) = \int \frac{p^+ dy^- d^2 y_\perp}{(2\pi)^3} e^{ixp^+ y^- - i\vec{k}_T \cdot \vec{y}_\perp} \langle A| \bar{\psi}(0) \frac{\vec{p}}{2k_T^2} \mathcal{L}(0; y) \psi(y)|A\rangle, \tag{A2}
\]

\[
f_{q\perp}^{-1}(x, \vec{k}_T) = \frac{1}{M^2} \int \frac{p^+ dy^- d^2 y_\perp}{(2\pi)^3} e^{ixp^+ y^- - i\vec{k}_T \cdot \vec{y}_\perp} \langle A| \bar{\psi}(0) \frac{\vec{p}}{2} \mathcal{L}(0; y) \psi(y)|A\rangle. \tag{A3}
\]

The corresponding collinear (\( \vec{k}_T \)-integrated) parton distribution and correlation functions, \( f_q^A(x) \) and \( f_{q\perp}^{-1}(x) \), can be obtained from the above by integration over \( \vec{k}_T \).

The following high-twist TMD parton distribution functions in terms of the matrix elements from both left and right cut diagrams in Fig. \([4]\)

\[
\varphi_{12}^{(i)A} = \frac{1}{2} \left( \varphi_{12}^{(i)LN} + \varphi_{12}^{(i)RN} \right), (i = 1, 2), \tag{A4}
\]

\[
\varphi_{12}^{(i)A} = \frac{1}{2} \left( \varphi_{12}^{(i)LA} + \varphi_{12}^{(i)RA} \right), (i = 1, 2), \tag{A5}
\]

where,
\[
\varphi^{(1,L)}_{\perp 2} = \int \frac{p^+ dy^- d^2 y_\perp e^{i\exp^+ y^- - i\vec{q}_\perp \cdot \vec{k}_\perp} (2k_{\perp;\alpha} k_{\parallel;\rho} - k_{\perp;\rho}^2 d_{\rho\alpha}) (A) |\bar{\psi}(0)\frac{\gamma_\alpha}{2} D_\alpha(0;y) L(0;y) \psi(y)| A, \\
\varphi^{(1,R)}_{\perp 2} = \int \frac{p^+ dy^- d^2 y_\perp e^{i\exp^+ y^- - i\vec{q}_\perp \cdot \vec{k}_\perp} (-ik_{\perp;\alpha} i\epsilon_{\rho\sigma})_\perp k_\perp^\sigma (A) |\bar{\psi}(0)\frac{\gamma_\alpha}{2} L(0;y) D_\rho(0) \psi(y)| A, \\
\varphi^{(2,L)}_{\perp 2} = \int \frac{dx_2}{x_2 - x - i\epsilon} \frac{dy^- d^2 y_\perp p^+ dz^- (2\pi)^3}{2\pi} \left( e^{ixp^+ z^- + i\exp^+ (y^- - z^-) - i\vec{q}_\perp \cdot \vec{y}_\perp - d_{\rho\alpha}} \right) k_\perp^\alpha \\
\times (A) |\bar{\psi}(0)\frac{\gamma^+}{2} L(0;z^- - 0, 0) D_\rho(z^-, 0, 0) L(z^-, 0, 0; y) \psi(y)| A, \\
\varphi^{(2,R)}_{\perp 2} = \int \frac{dx_1}{x_1 - x + i\epsilon} \frac{dy^- d^2 y_\perp p^+ dz^- (2\pi)^3}{2\pi} \left( e^{ixp^+ z^- + i\exp^+ (y^- - z^-) - i\vec{q}_\perp \cdot \vec{y}_\perp - d_{\rho\alpha}} \right) k_\perp^\alpha \\
\times (A) |\bar{\psi}(0)\frac{\gamma^+}{2} L(0;z^- + 0, 0) D_\rho(z^-, 0, 0) L(z^-, 0, 0; y) \psi(y)| A, \\
\varphi^{(2,R)}_{\perp 2} = \int \frac{dx_2}{x_2 - x + i\epsilon} \frac{dy^- d^2 y_\perp p^+ dz^- (2\pi)^3}{2\pi} \left( e^{ixp^+ z^- + i\exp^+ (y^- - z^-) - i\vec{q}_\perp \cdot \vec{y}_\perp - d_{\rho\alpha}} \right) k_\perp^\alpha \\
\times (A) |\bar{\psi}(0)\frac{\gamma^+}{2} L(0;z^-, y_\perp) D_\rho(z^-, y_\perp) L(z^-, y_\perp; y) \psi(y)| A,
\]

where \( d^{\mu\nu} = g^{\mu\nu} - \vec{n}^{\mu}_{\perp} \nu - \vec{n}^{\nu}_{\perp} \mu \), \( \epsilon^{\mu\nu\sigma\rho} = \epsilon^{\mu\nu\sigma\rho} \delta_{\rho\sigma} \) and \( \epsilon^{\mu\nu\rho} \) the anti-symmetric unit tensor. The four-vector of the transverse momentum is defined \( k_\perp = (0, 0, k_\perp) \).

In the calculation of the \( \vec{k}_\perp^2 \)-weighted differential cross section, the following collinear parton distribution and correlation functions are used.

\[
\langle \vec{k}_\perp^2 f_q^A \rangle (x) = \int d^2 \vec{k}_\perp \vec{k}_\perp^2 f_q^A (x, \vec{k}_\perp) \\
= \int \frac{dy^- d^2 y_\perp d^2 \vec{k}_\perp e^{i\exp^+ y^- - i\vec{q}_\perp \cdot \vec{y}_\perp} \vec{k}_\perp^2 (A) |\bar{\psi}(0)\frac{\gamma^+}{2} L(0;y) \psi(y)| A, \\
\langle \vec{k}_\perp^2 f_{q(-)}^A \rangle (x) = \int d^2 \vec{k}_\perp \vec{k}_\perp^2 f_{q(-)}^A (x, \vec{k}_\perp) \\
= \frac{p^+}{M^2} \int \frac{dy^- d^2 y_\perp d^2 \vec{k}_\perp e^{i\exp^+ y^- - i\vec{q}_\perp \cdot \vec{y}_\perp} \vec{k}_\perp^2 (A) |\bar{\psi}(0)\frac{\gamma^+}{2} L(0;y) \psi(y)| A, \\
\langle \vec{k}_\perp^4 \varphi^{(2,L)}_{\perp 2} \rangle (x) = \int \frac{d^2 \vec{k}_\perp dx_2 dx_1 \frac{dy^- d^2 y_\perp p^+ dz^- (2\pi)^3}{2\pi} e^{ixp^+ z^- + i\exp^+ (y^- - z^-) - i\vec{q}_\perp \cdot \vec{y}_\perp} (d_{\rho\alpha} \vec{k}_\perp^\alpha) \\
\times (A) |\bar{\psi}(0)\frac{\gamma^+}{2} L(0;z^- - 0, 0) D_\rho(z^-, 0, 0) L(z^-, 0, 0; y) \psi(y)| A,
\]
\begin{align}
\langle \bar{K}_L \varphi_{\perp}^{(2,R)A}(x) \rangle &= \int \frac{d^2 \vec{k}_L}{x_1 - x + i \epsilon} \frac{dy_\perp dy_\parallel p^+ dz^-}{2\pi^3} e^{ixp^+ z^- + ix_1 p^+(y^- - z^-) - i\vec{k}_L \cdot \vec{y}_\perp} (d_\sigma^\perp k_L^2) \\
&\times \langle A | \bar{\psi}(0) \gamma^+ \hbar_0 (0; z^- , y_\perp) D_\rho(z^- , y_\perp) D_\sigma(z^- , y_\perp) \mathcal{L}(z^- , y_\perp; y) \psi(y) | A \rangle, \\
\langle \bar{K}_L \varphi_{\perp}^{(2,L)A}(x) \rangle &= \int \frac{d^2 \vec{k}_L}{x_2 - x - i \epsilon} \frac{dy_\perp dy_\parallel p^+ dz^-}{2\pi^3} e^{ix_2 p^+ z^- + ix_1 p^+(y^- - z^-) - i\vec{k}_L \cdot \vec{y}_\perp} (i\epsilon_\perp^\rho k_L^2) \\
&\times \langle A | \bar{\psi}(0) \gamma^+ \hbar_0 (0; z^- , y_\perp) D_\rho(z^- , y_\perp) D_\sigma(z^- , y_\perp) \mathcal{L}(z^- , y_\perp; y) \psi(y) | A \rangle, \\
\langle \bar{K}_L \varphi_{\perp}^{(2,R)A}(x) \rangle &= \int \frac{d^2 \vec{k}_L}{x_1 - x + i \epsilon} \frac{dy_\perp dy_\parallel p^+ dz^-}{2\pi^3} e^{ixp^+ z^- + ix_1 p^+(y^- - z^-) - i\vec{k}_L \cdot \vec{y}_\perp} (i\epsilon_\perp^\rho k_L^2) \\
&\times \langle A | \bar{\psi}(0) \gamma^+ \hbar_0 (0; z^- , y_\perp) D_\rho(z^- , y_\perp) D_\sigma(z^- , y_\perp) \mathcal{L}(z^- , y_\perp; y) \psi(y) | A \rangle. 
\end{align}

In the calculation of the $\vec{k}_L$-integrated differential cross section, one also encounters the following collinear parton correlation functions,

\begin{align}
\psi_{\perp}^{(2)A}(x) &= \frac{1}{2} \left[ \langle \bar{K}_L \varphi_{\perp}^{(2,L)A}(x) \rangle + \langle \bar{K}_L \varphi_{\perp}^{(2,R)A}(x) \rangle \right] \\
&= ip^+ \int \frac{dy^-}{4\pi} \int_0^{y^-} dz^- e^{ixp^+ y^-} \langle A | \bar{\psi}(0) \gamma^+ \hbar_0 (0; z^-) D_\rho^2(z^-) \mathcal{L}(z^-; y^-) \psi(y^-) | A \rangle, \\
\psi_{\perp}^{(2)\bar{A}}(x) &= \frac{1}{2} \left[ \langle \bar{K}_L \varphi_{\perp}^{(2,L)A}(x) \rangle + \langle \bar{K}_L \varphi_{\perp}^{(2,R)A}(x) \rangle \right] \\
&= -p^+ \int \frac{dy^-}{4\pi} \int_0^{y^-} dz^- e^{ixp^+ y^-} \epsilon_\perp^\rho \langle A | \bar{\psi}(0) \gamma^+ \hbar_0 (0; z^-) D_\rho(z^-) D_\sigma(z^-) \mathcal{L}(z^-; y^-) \psi(y^-) | A \rangle. 
\end{align}

Since nucleons are color singlet states, the quark field operators in the above matrix elements must operate on a single nucleon inside the nucleus. This limits the range of the coordinate $y^-$ to the size of a nucleon, which also limits the range of $z^-$ integration. Therefore, the above matrix elements should be proportional to the atomic number of the nucleus and do not have any extra nuclear enhancement.

All the matrix elements defined above for nuclear states are also valid for a nucleon. The $\vec{k}_L$-weight-integrated nuclear parton correlation functions $\langle \bar{K}_L \varphi_{\perp}^{(2,A)}(x) \rangle$ and $\langle \bar{K}_L \varphi_{\perp}^{(2,B)}(x) \rangle$ are also related to the parton correlation functions in Eqs. (A20) and (A21) for a nucleon as shown in Sec. III.
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