Optimal Kinetic Parameters of Trickle bed Reactor for Oxidation of 2-Proplymercaptan in Naphtha

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Abstract

The best kinetic of the reaction are estimated based on experimental data obtained from the literature using parameter estimation technique. The best mathematical model for oxidative 2-propylmercaptan via oxygen is taking into account the apparent intrinsic kinetics considering internal diffusion and TBR hydrodynamic effect on the reaction process mainly, catalyst wetting efficiency, catalyst effectiveness factor, Thiele model and the effective diffusivity. The optimal operating condition for oxidative process is carried out utilizing. The optimization technique based upon the minimization of the sum squared error between experimental and predicted composition of naphtha oxidative process to determine the best parameters of kinetics models. The predicted product compositions for oxidation process found to be a good agreement with the experimental data for wide range of operating conditions (2.5-10 hr⁻¹, 75-300 ppm and 293-353K) with minimum error 5% among all results.

Keywords: Naphtha oxidation, Trickle bed reactor, Mathematical modeling, Optimization

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Introduction

The deep-ultra-desulfurization of feedstock with low sulfur compounds content has been a major concern in petroleum industries due to in the stringent statutory regulations imposed by the government worldwide [1]. Environmental concerns have driven to remove sulfur compounds containing (mercaptans, sulfide, disulfide and thiophene) from fuel because such compounds lead to produce precursors to acid rain by sulfur oxides and airborne particulate material [2]. The catalysts and other types of oxidizer used in oxidation desulfurization process (ODS) should be very high selective to organic sulfur compounds. Sulfur compounds are known to be slightly more polar than hydrocarbon compounds to prevent the oxidation of olefins or aromatic compounds present in the feedstock [3]. The process of catalytic oxidation desulfurization is commonly used for sulfur removal from fuels [4].

Removing sulfur by oxidation process has received considerable attention owing to the advantages or characteristics of such process. The biggest advantage of this shortage of oxygen-depleting substances is that this process can be carried out under moderate conditions of low temperature and atmospheric pressure. These characteristics distinguish them from the HDS process. Also, the important sulfur compounds tend more reactive to the oxidation process than HDS process. The oxidation process (ODS) is a chemical reaction by catalyst and oxidant leads to form of sulfoxide or sulfones. The oxidized compounds can be removed from oil using non-miscible solvent and choosing the conventional separation method, such as extraction, adsorption or distillation [5].

The oxidants for oxidative desulfurization process (ODS) include nitric acid (HNO₃) [6], hydrogen peroxide (H₂O₂)[7], air[8], oxygen (O₂) [9] and ozone (O₃) [10]. The primary criteria in choosing an appropriate oxidant for ODS process is the active oxygen content as the ratio between the weight of oxygen that can be transfer to sulfur compound, and the molecular weight of oxidant, oxidant cost, selectivity associate to its use in sulfur oxidant, environmental effect (by product), and the necessity to make oxidant recovery and the use of gas oxidant (O₂ and air for example) needs not to make oxidant recovery [11].

There are study on oxidative desulfurization of 2-propylmercaptan. Recently, Yassin (2010) [12] developed a mathematical model to investigate theoretical analysis and the performance evaluation for trickle bed reactor process. They compared predictions results with experimental data obtained from trickle bed reactor in oxidation process. They considered a steady state process parametric study and the results showed that an increase in reaction temperature with decreasing in liquid hour space velocity, high conversion was obtained from 2-propylmercaptan oxidative.

However, the model developed by them have described the oxidation process of trickle bed reactor with ignoring most of the parameters affecting the trickle bed reactor, mainly wetting efficiency, internal diffusion and so on. Also, fixed kinetic parameters have been assumed (1st or 2nd order) making the kinetic behavior is not accurate in such oxidation process in addition to the physical properties. Thus, in this study, the optimal kinetic parameters is investigated here in order to obtain the best kinetic parameters of naphtha oxidative with high accuracy and then such optimal parameters can be applied confidently to reactor design operation and conditions. This study aims to develop a new mathematical modeling of trickle bed reactor for naphtha oxidative process related to 2-propylmercaptan in naphtha. The mathematical modeling has developed based upon the pilot plant experiment with a homemade catalyst (2%Co/AC) for oxidative desulfurization of 2-propylmercaptan in naphtha, under moderate operating conditions using oxygen as the oxidant for 2-propylmercaptan.
been used for modeling, simulation and parameter estimation via optimization. The optimization problem is posed as a nonlinear programming (NLP) and is solved using successive quadratic programming (SQP) method within the gPROMS packing. Graphical abstract as shown in the Figure below.

Experimental Data

The experimental data used in this process has taken from Yassin (2010) [12]. Mathematical Modeling
A heterogeneous one dimensional (axial dispersion) model including a set of mass balances equation as well as kinetics equations is taken is consideration. In the trickle bed reactor, oxidative of RSH-C3 in naphtha by oxygen flow is carried out. The reaction is as follows [14], mercaptan oxidizes to disulfide directly.

\[ \text{RSH} + \text{Oxidant} \rightarrow \text{RSSR} \]

The following assumptions in the mathematical modeling of trickle bed reactor were used in this study:
- The feedstock (naphtha) is saturated with gas inlet (pure oxygen) at all times and gaseous reactant present in large excess.
- The oxidation reaction occurs in axial direction.
- The reaction is assumed to occur only in porous solid.
- Isothermal operation for trickle bed reactor.
- No evaporation or condensation occurs from or into the liquid phase.

• **Trickle Bed Reactor with Co-current Gas-Liquid Interface**

A trickle bed reactor (TBR) consists of a column that very high (length of TBR), equipped with one or various fixed beds of solid catalysts used in oxidation reaction in the refinery, throughout which gas (Pure O\textsubscript{2}) and feedstock liquid (naphtha) move in co-current down flow. Show in the Figure 1. The typical film flow texture found during a trickle-flow regime [40]. In this mode, oxygen is the continuous phase and liquid (naphtha) holdup is lower. This operation is the one most used in practice, since there are less severe limitations in throughput than in counter cur-rent operation.
Figure 1: Distribution of feedstock (Naphtha and Oxygen) above the catalyst surface in (TBR).

Mass Balance

The differential equations for oxidation process describing mass balance in the axial direction of a trickle bed reactor are expressed by the following subsections:

Mass balance for catalytic reactor over 2-proplymercaptan compounds entering the trickle bed reactor is follow [15]. Representation of equations in the TBR is show in Figure 2.

\[
\begin{align*}
\text{Mole flux of} & \ (\text{RSH-C3}) \ \text{Input} \times \text{Cross section area of reactor} - \\
\text{Mole flux of} & \ (\text{RSH-C3}) \ \text{Output} \times \text{Cross section area of reactor} - (\text{Accumulation}) - (\text{Generation by Reaction}) = 0 \\
\left(\text{Input of} \ (\text{RSH-C3}) \times A\right) - (\text{Output of} \ (\text{RSH-C3}) \times A) - (\text{Accumulation}_{\text{(RSH-C3)}}) - (\text{Generation by Reaction}_{\text{(RSH-C3)}}) = 0
\end{align*}
\]

Figure 2: Representation of equations in the Trickle Bed Reactor for oxidation process
Generation by Reaction \( R_{\text{SH}-C3} \) =  
\[-R_{\text{SH}-C3}dV_{\text{reactor}} \]  
(c) 

\[ N_A = \text{Mole flux of 2 - RSH} \]  
\[ A_{\text{reactor}} = \text{Cross section area of reactor} \]  
\[ \text{Reaction area =} \pi r^2 \text{reactor} \]  
(d) 

Accumulation by reaction for mercaptan oxidation reaction=0 

Substitution of a,b,c & d in equation 2 we get,  
\[ (N_{\text{SH}-C3} \times \pi r^2 \text{reactor}) - \left( (N_{\text{SH}-C3} + dN_{\text{SH}-C3}) \times \pi r^2 \text{reactor} \right) = (-R_{\text{SH}-C3})dV \]  
(3) 

\[ (N_{\text{RSH}-C3} \times \pi r^2 \text{reactor}) - \left( (N_{\text{RSH}-C3}) + dN_{\text{RSH}-C3} \times (1 - X_{\text{RSH-C3}}) \right) \times \pi r^2 \text{reactor} = \]  
\[ (-R_{\text{RSH-C3}})dV \]  
(4) 

\[ (N_{\text{RSH-C3}} \times \pi r^2 \text{reactor}) - \left( (N_{\text{RSH-C3}}) - N_{\text{RSHO-C3}} \times X_{\text{RSH-C3}} \right) \times \pi r^2 \text{reactor} = \]  
\[ (-R_{\text{RSH-C3}})dV \]  
(5) 

\[ (N_{\text{RSHO-C3}} \times X_{\text{RSH-C3}} \times \pi r^2 \text{reactor}) = \]  
\[ (-R_{\text{RSH-C3}})dV \]  
(6) 

- The Chemical Reaction Rate \(-R_{\text{RSH-C3}}\)
  The chemical reaction rate \(-R_{\text{RSH-C3}}\) and the mechanism of mercaptans oxidation has been reported by some researchers [39], in the presence of an oxidation-reduction catalyst, reactor occurs by an anion-radical mechanism. First forming mercapride ions \( RSH -> RSH^{-1} + H^{+1} \) 

Oxygen can react with the cation by one electron transfer reaction to produce peroxy ion leading to high oxidation state of the cation.  
\[ 2M^{+2} + O_2 \rightarrow 2M^{+3} + O_2^{-2} \]  

Regeneration of the catalyst occurs by one electron transfer reaction between the mercaptide ion and the oxidized cation.  
\[ 2RS^{-1} + 2M^{+3} \rightarrow 2M^{+2} + 2RS^{+} \]

The resulting thyl radicals dimerize, and the peroxy ion is destroyed by the next reaction with water.  
\[ 2RS^{+} \rightarrow RSSR \]

Finally, hydroxide ions react with proton leading to form water molecule as follows.  
\[ O_2^{-1} + H^{+1} \rightarrow H_2O \]

The chemical reaction and the mechanism of mercaptans as shows in the Figure 3. 

The chemical reaction of oxidation 2-propylmercaptan in naphtha \(-R_{\text{RSH-C3}}\) by oxygen using trickle bed reactor (TBR) may be reasonably taken into consideration assuming \( n^{th} \) order kinetics for hydrodynamic processing for all behavior occur in the TBR for oxidation of 2-propylmercaptan using oxygen.  
\[ -R_{\text{RSH-C3}} = K_{\text{Hyd}}C_{\text{RSH-C3}}^n \]  
(7) 

The hydrodynamic effects and internal diffusion is taken in the reaction based on apparent kinetics as follows [16, 17]:  
\[ K_{\text{Hyd}} = \text{Rate constant} \times \text{Effectiveness factor} \times \]  
\[ \text{Wetting efficiency} \]

\[ K_{\text{Hyd}} = K_{\text{RSH-C3}} \times \psi_{\text{Eff}, \text{fact}} \times \psi_{\text{Wett}, \text{fact}} \]  
(8) 

Where: \( \psi_{\text{Wett}, \text{fact}} \), \( \psi_{\text{Eff}, \text{fact}} \) are the catalyst wetting efficiency and effectiveness factor, respectively.

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Figure (3): The chemical reaction and the mechanism of mercaptans. 

The reaction rate equation for oxidation 2-propylmercaptan is stated as 
\[ \left( -R_{\text{RSH-C3}} \right) = K_{\text{RSH-C3}} \times \psi_{\text{Eff}, \text{fact}} \times \psi_{\text{Wett}, \text{fact}} \times C_{\text{RSH-C3}}^n \]
\[-R_{(RSH-C3)} = - \frac{dC_{(RSH-C3)}}{dt} = K_{(RSH-C3)} \cdot \Psi_{Eff.fact.} \cdot \Psi_{Wett.fact.} \cdot C_{(RSH-C3)}^{n} \quad (9)\]

The general behavior can be stated as, higher conversion is achieved at higher temperature due to the fact that at higher temperature, kinetic constant (rate constant) is favorably affected resulting in increasing in 2-propylmercaptan conversion.

Reaction rate constant \(K_{(RSH-C3)}\) can be described by Arrhenius equation as follows [19]:
\[K_{(RSH-C3)} = A_0 e^{-\frac{E_A}{RT}} \quad \ldots \quad (10)\]

Substation equation 10 in equation 9, we get:

The catalytic reaction of 3-propylmercaptan of oxidation by \(n^{th}\) order kinetic substituted equations is integrated and giving the following final expression:
\[(-R_{RSH-C3}) = \frac{dC_{(RSH-C3)}}{dt} = A_0 e^{-\frac{E_A}{RT}} \cdot \Psi_{Eff.fact.} \cdot \Psi_{Wett.fact.} \cdot C_{(RSH-C3)}^{n} \quad \ldots \quad (11)\]

\[\tau = \int_{0}^{X_{RSH-C3}} A_0 e^{-\frac{E_A}{RT}} \cdot \Psi_{Eff.fact.} \cdot \Psi_{Wett.fact.} \cdot C_{(RSH-C3)}^{n} \quad \ldots \quad (12)\]

The conversion of 2-propylmercaptan to disulfide.
\[X_{RSH-C3} = \frac{C_{RSH-C3}}{C_{RSH-O}} \quad \ldots \quad (13)\]

\(LHSV\): is the ratio of the hourly volume of oil processed to the volume of the catalyst used in oxidation process.

\[LHSV (hr^{-1}) = \frac{1}{\tau} = \frac{volume \ of \ catalyst (m^{3})}{volume \ to \ the \ reactor (m^{3})} \quad = \frac{\dot{Q}_L}{V} \quad \ldots \quad (14)\]

Integration equation becoming:
\[\tau K_{Hyd} = \frac{\dot{Q} (RSH-C3) K_{Hyd}}{V} = \frac{1}{n-1} \left( \frac{1}{C_{RSHf-C3}} - \frac{1}{C_{RSH0-C3}} \right) \quad (15)\]

\[\tau K_{(RSH-C3)} \cdot \Psi_{Eff.fact.} \cdot \Psi_{Wett.fact.} = \frac{1}{n-1} \left( \frac{1}{C_{RSHf-C3}} - \frac{1}{C_{RSH0-C3}} \right) \quad (16)\]

\[\frac{1}{K_{(RSH-C3)} \cdot \Psi_{Eff.fact.} \cdot \Psi_{Wett.fact.}} LHSV = \frac{1}{n-1} \left( \frac{1}{C_{RSHf-C3}} - \frac{1}{C_{RSH0-C3}} \right) \quad (17)\]

* The catalyst wetting efficiency \(\Psi_{Wett.fact.}\).

The catalyst wetting efficiency \(\Psi_{Wett.fact.}\) of the external catalyst surface can be calculated based on the atmosphere pressure (in this process at 1 bar) as a function for modified Reynolds number and modified Galileo number using the following correlation [19, 15and 17]:

**For Ideal**: Complete wetting for catalyst used in the oxidation reaction as show in Figure 4a.

**For Non-Ideal**: Complete wetting for catalyst used in the oxidation reaction as show in Figure 4b.

\[\text{Figure 4a: Wetting efficiency for ideal process.}\]

The wetting efficiency \(\Psi_{Wett.fact.}\) did not complete wetting in the trickle bed reactor (TBR) for non-ideal wetting.
\[ \psi_{\text{Wett.fact.}} = 1.617 \left( \frac{\rho_{\text{naphtha}}}{\rho_{\text{nap}}^{1-e_{\text{Void}}}} \right)^{0.146} \]
\[ = \left[ \frac{\rho_{\text{naphtha}}^3 e_{\text{Void}}^3}{\rho_{\text{naphtha}}(1-e_{\text{Void}})} \right]^{0.071} \]

\[ (18) \]

Figure 4b: Wetting efficiency for non-ideal process.

- The Porosity or void fraction \( e_{\text{Void}} \)

The Porosity or void fraction \( e_{\text{Void}} \) of the catalyst is a measure of the void (i.e. ‘empty’) spaces in a material, and is a fraction of the volume of voids over the total volume. The catalyst is estimated for undiluted sphere packed catalyst using in the trickle bed reactor from the following equation [20, 21 and 22]. The void fraction and porosity in particle is show in Figure 5.

\[ e_{\text{Void}} = \frac{\text{Volume of voids in the bed}}{\text{total volume of bed}} \]  
\[ (19a) \]

\[ e_{\text{Void}} = 0.453 + 0.037 \left( \frac{D_t - 2D_{pe}}{D_t} \right)^2 \]  
\[ (19b) \]

\( D_{pe} \): Equivalent particular diameter, which is defined as the diameter of the sphere that has the same external surface (or volume) as the actual catalyst particle. It is an important particle characteristic that depends on the particle size and shape.

Figure 5. Void fraction and porosity forms in packed bed and particle respectively.
\[
\varepsilon_{\text{void}} = 0.453 + 0.037 \left( \frac{D_t - 2D_p}{D_t} \right)^2 \quad (20)
\]

- Density of Naphtha [\(\rho_{\text{naphtha}}\)]

The density of Naphtha as a function of temperature has been proposed by the following generalized equation to calculate the density of liquids as shown below [23, 24]:

\[
\rho_{\text{naphtha}} = \left( \frac{P_C \cdot MW_{\text{naphtha}}}{RT_C \cdot (1 + (1 - T_r))^{0.2857}} \right) \quad (21)
\]

\[
Z_C = \frac{P_C \cdot V_C}{RT_C} \quad (22)
\]

- Critical pressure of naphtha, psia

\[
P_C: \text{Critical pressure of naphtha, psia}
\]

\[
MW_{\text{naphtha}}: \text{Molecular weight of naphtha, lb mol}^{-1}
\]

- Gas constant, \(ft^3\) psia lb mol \(^{-1}\) \(R\)

\[
T_C: \text{Critical temperature of naphtha, R}^\circ
\]

- Critical compressibility factor, \(T_r\)

\[
Z_C: \text{Critical compressibility factor,} = -
\]

- Reduced temperature, \(-\)

\[
V_C: \text{Critical molar volume, ft}^3 \text{lb mol}^{-1}
\]

- Viscosity of Naphtha [\(\mu_{\text{naphtha,b}}\)]

The viscosity of naphtha depends mainly on the temperature (inversely proportion), thus, it is particularly desirable to determine liquid viscosities from experimental data when such data exist. Many correlations were used to calculate liquid viscosity and one of the best correlations that have widely been applied in calculating liquid viscosity [24, 25].

\[
ln \mu_{\text{naphtha}} = \left[ \frac{ln \mu_{\text{naphtha,b}}}{ln(\alpha \cdot \mu_{\text{naphtha,b}})} \right]^\varphi \ln(\alpha \cdot \mu_{\text{naphtha,b}}) \quad \ldots (23)
\]

- Volume fraction of molecule \(\varphi\)

\[
\varphi = \left( \frac{1 - T_r}{1 - T_{br}} \right) \quad (24)
\]

\[
T_r = \left( \frac{T}{T_C} \right) \quad (25)
\]

\[
T_{br} = \left( \frac{T}{T_C} \right) \quad (26)
\]

- Effectiveness factor \([\Psi_{\text{Eff.fact.}}]\)

The effectiveness factor \([\Psi_{\text{Eff.fact.}}]\) can be determined as a function of Thiele modulus \(\Theta\) with the following equation valid for sphere particles [26]:

\[
\Psi_{\text{Eff.fact.}} = \frac{3}{2} \left[ \frac{\Theta \sinh \Theta - \cosh \Theta}{\cosh \Theta} \right] \quad (27)
\]

Effectiveness factor as a function of Thiele modulus for different geometries of catalysts are show in semi log flow sheet in the Figure 6.

- Thiele Diffusion Modulus [\(\Theta\)]

For \(n^{th}\) order for oxidation irreversible reaction, the general Thiele Modulus (\(\Theta\)) is evaluated using the following relationship [27]:

\[
\Theta = \frac{\theta}{r_{\text{diffusion}}}
\]

Rate of react is a function of (volume of shell, surface area of pores per volume catalyst and rate per area catalyst).

Representation of mathematical model for particle catalyst of Thiele diffusion modulus is show in the below figure.

![Image](Image)
Figure 6: Effectiveness factor as a function of Thiele modulus for different geometries of catalysts.

- Effective diffusivity $[D_{ei}]$

  
  $D_{ei} = (J \cdot \varepsilon_s) \left( \frac{D_{mi}}{\varepsilon_s} + \frac{D_{ki}}{\varepsilon_s} \right)$  \hspace{1cm} (31)

  Catalyst Porosity $\varepsilon_s$, Catalyst particle porosity can be calculated using simple equation below depending on the particle density and pore volume. Show in Figure 8.

  $\varepsilon_s = \frac{\rho p}{\rho L}$  \hspace{1cm} (32)

  The effective diffusivity inside the catalyst particle includes two diffusion contributions: Knudsen diffusivity $[D_{ki}]$ and Molecular diffusivity $[D_{mi}]$.

  
  Rate per area catalyst = $K_{Hyd}$  \hspace{1cm} (33)

Knudsen diffusivity is Known in this equation [15, 17] based on Mean pore radius:

  $D_{ki} = 9700 \left( \frac{2 \nu g^2}{8g} \right) \left( \frac{T_{meABP}}{T} \right)^{1/2}$  \hspace{1cm} (33)

Molecular diffusivity:

  The Molecular diffusivity of naphtha can be calculated with respect to following equation:

  $D_{mi} = 8.93 \times 10^{-8} \left( \frac{\nu_{RSH-C3}^{0.267}}{\nu_{RSH-C3}^{0.048}} \right)$  \hspace{1cm} (34)

$\nu_{RSH-C3}$ Molar volume of 2-proplymercaptan in naphtha, can be calculated by the following equation with respect to correlation [32].

  $\nu_{RSH-C3} = 0.285\nu_{L}$  \hspace{1cm} (35)

  The critical specific volume of liquid (naphtha) is estimated by correlation [33].

  Surface area of particles of catalyst = $4\pi(R_p)^2$

  $v_{naphtha} = (7.5214 \times 10^{-3}(T_{meABP})^{0.286}(\beta_{15.6})^{-0.7666})MW_L$ ...
Mean average boiling point = 
Volume average boiling point − Δ 

\[ M_{ABP} = V_{ABP} - \Delta \]  

\[ V_{ABP} = (T_{30} + T_{50} + T_{70} + T_{90}) \]  

\[ \Delta = \frac{(T_{90} - T_{10})}{(90 - 10)} \] 

- The tortuosity factor \((\bar{J})\) 

The tortuosity factor \((\bar{J})\) of the pore network, is used in the calculation of \(D_{el}\) because the pores are not oriented along the normal direction from the surface to the center of the catalyst particle [34]: 

\[ \bar{J} = \frac{2 \log(\epsilon_s)}{2\pi} \]  

The Trickle Bed Reactor process model for oxidation reaction of naphtha (Equations 1–40) is developed and solved within the gPROMS package. Parameters used in the mathematical model for oxidation reaction are shown in Table 1.

| 0  | Symbol & Value                      | Unit  |
|----|------------------------------------|-------|
| 1  | Initial concentration               | ppm   |
| 2  | Temperature                         | K     |
| 3  | Liquid hour space velocity          | hr⁻¹  |
| 4  | Gas molecular constant              | J/mol.K, atm.lit./mol.K,  
                                           |       |
| 5  | Molecular weight of naphtha         | g/mol |
| 6  | Molecular weight of oxygen          | g/mol |
| 7  | Tube diameter                       | cm    |
| 8  | Bulk density                        | g/cm³ |
| 9  | Critical specific volume of         | ft³/mol|
|    | the 2-propylmercaptan compound      |       |
| 10 | Velocity of naphtha                 | cm/sec|
| 11 | Acceleration gravity                | cm/s² |
| 12 | Total pore volume                   | cm³/g |
| 13 | Total geometric surface             | cm²   |
|    | area of catalyst particle           |       |
| 14 | Total geometric volume of           | cm³   |
|    | catalyst particle                   |       |
| 15 | Critical pressure of naphtha        | Psia  |
| 16 | Specific surface area               | cm²/g |
| 17 | Diameter of catalyst particle       | cm    |
| 18 | Pressure                            | Psia  |
| 19 | Mean average boiling point          | R     |
| 20 | Critical temperature of naphtha     | R     |

Estimation of Kinetic Parameters of the Model

For solving the set of ordinary differential equations (ODEs) (for the steady-state regime) or the set of PDEs (for the dynamic regime) presented of oxidation reaction, it is important to estimate a lot of the parameters and chemical properties of the system. Those parameters can be evaluated with existing correlations, whose accuracy is of great importance for the entire state of robustness of the reactor model. Estimation of kinetic parameters is an important and difficult step in the development of models, calculations of unknown kinetic parameters can be achieved by utilizing experimental data. When estimating kinetic parameters of the models, the goal is to calculate appropriate parameter values so that errors between experimental and theoretical data (based on mathematical model) are minimized. The kinetic modeling of oxidation reaction by oxygen process using the following objective function based upon the minimization of the sum of squared errors (SSE) between the experimental concentrations of 2-propylmercaptan \((C_{RSH-C3}^{Exp})\) and predicted \((C_{RSH-C3}^{Pred})\). For parameter estimation, the objective function (OBJ), as given below, was minimized:

\[ OBJ = \sum_{n=1}^{N_c} (C_{RSH-C3}^{Exp} - C_{RSH-C3}^{Pred})^2 \]

It is known that the predicted conversion of 2-propylmercaptan can be calculated from the following equation:

\[ X_{RSH-C3} = \frac{C_{RSH-C3} - C_{RSH-C3}^{Exp}}{C_{RSH-C3}^{Exp}} \]

Optimization Problem Formulation for Parameter Estimation

Mathematically, the optimization problem can be described as:

\[ \text{Min} \quad \text{SSE} \]

\[ N_c \quad K_j, \quad (i=1-4, \quad j=\text{Cobalt/Activated carbon}) \]

\[ \text{St.F} (x, \quad z, \quad x (z), \quad u (z), \quad v) = 0 \]

\[ C_i \leq C \leq C_U \]

\[ N_l \leq N \leq N_U \]

\[ K_i \leq K_j \leq K_U \]

\[ K_i \leq K_j \leq K_U \]
The activation energy of 2-propylmercaptan found in the current work is in agreement with that found in the literature, which is (15.88kJ/mole) using formic acid/H₂O₂ as the phase transfer catalyst[35]. However, Huang [36] has found that the activation energy of sulfur is (28.7 kJ/mole) using H₂O₂ as oxidant and poly tetrafluoro ethylene as catalyst system. Also, the solvent used in the process of oxidation reaction can effect on the activation energy, as well as the type of sulfur using in the processing.

Change of 2-Propylmercaptan Phase

The temperature used in oxidation reaction is increasing from 293 to 353 K, phase changes of in feedstock is found including sulfur content (2-propylmercaptan) from liquid to vapor boiling range of 2-propylmercaptan equal to 326 K, causing the oxidation reaction of 2-propylmercaptan in naphtha to be more active at vapor phase due to high diffusivity rate of molecules inside catalyst pores. While another mercaptan in the feedstock throughout oxidation reaction does not effect on the mercaptan phase through temperature change, where (n-butly mercaptan having boiling point of 373K) this mercaptan does not change the phase when temperature changes from 293 to 353K. This agrees with findings of Xia [14], which showed a positive effect of temperature with conversion of OSCs and disagrees with respect to Gheni [13] that showed an increase in conversion when the temperature increased from 293 to 313 K.
Effect of Temperature on Oxidation Process

Figure (9) shows the effect of temperature on the oxidation of 2-propymercaptan at different liquid hour space velocity. The conversion of 2-propymercaptan is increasing with increasing the temperature from 333 to 353 K at constant liquid hour space velocity of 2.5 hr⁻¹ as shown in Figures (9a, 9b, 9c) at LHSV of 2.5 hr⁻¹ and different initial concentration of 2-propymercaptan (a = 300 ppm, b = 150 ppm, c = 75 ppm). It has been observed based on the results obtained that the predicted product conversion showed very good agreement with the experimental data for a wide range of operating conditions. Such behavior (higher conversion) is achieved at higher temperature due to the fact that at high temperature, kinetic constant (reaction rate constant) is favorably affected resulting in increasing in 2-propymercaptan conversion. The increase in the temperature level will contribute to an increase of magnitudes of some important physical properties (diffusivity and Henrys constant and mainly, decreasing in the viscosity and surface tension). However, the increase in the temperature of the oxidation process will raise the absorption rate of molecular oxygen in the liquid at the diffusion rate of sulfur compound, and the rate dissolved oxygen in the side catalyst, leading to format oxidation reaction[15, 17 and37].
Figure 9: Effect of temperature on 2-propymercaptan conversion. Reaction conditions (initial 2-propymercaptan concentration, (a)=300 ppm, (b)=150 ppm, (c)=75 ppm at 2.5 hr⁻¹).

Impact of Initial 2-Propymercaptan Concentration on Oxidation Reaction

The impact of initial concentration on the 2-propymercaptan conversion has studied in the range (300, 150, 75 ppm) with other parameters (LHSV and temperature). The comparison between the experimental data and the predicted data is plotted in the Figure (10) and a good agreement between the experimental results and predicted data have been obtained. In the range of such experiments, sulfur conversion is decreasing as decreased in the inlet sulfur concentration as shows in the Figure (11). It has been noticed that the sulfur conversion decreased from 74.7% to 68.2% at the same operating condition at 353K and 2.5 hr⁻¹ for inlet sulfur of 300 to 75, respectively. When decreases the sulfur molecular coverage active site over the catalyst surface leads to decrease the activation of the oxidation reaction [38].
Figure 10: Effect of initial 2-Proplymercaptan concentration on conversion. Reaction conditions (temperature= 353K, liquid hourly space velocity = 2.5hr⁻¹).

Figure 11: Effect of initial 2-Proplymercaptan concentration on conversion. Reaction conditions (Change of Temperature and constant liquid hour space velocity 2.5hr⁻¹).

Effect of Liquid Hour Space Velocity on Oxidation Process

The effect of liquid hour space velocity on 2-proplymercaptan removal rate was studied in the range (2.5, 3.33, 5, 10 hr⁻¹). The comparison between the experimental and predict results are plotted in Figures (12and13).

As shows in these Figures an increase in liquid hour space velocity or decrease in naphtha volumetric flow rate, cause

shorting in contact time between reactant material and catalyst particles [38]. Thus, effect the oxidation reaction causes the decrease in 2-proplymercaptan conversion. The increase in liquid hour space velocity can also effect on catalyst wetting radial and axial dispersion and liquid hold up. The conversion of 2-proplymercaptan at 353 K is 73.8% has achieved at 2.5 hr⁻¹, whereas the conversions decreases as increasing in LHSV for 2-proplymercaptan up to 26.7%, 22%, 16%and 8% at LHSV 2.5,3.33, 5 and 10 hr⁻¹ respectively, as shows in the Figure(13).
Comparison between Experimental and Simulation Results

The comparison between the experimental and predicted results is shown in the Figure(14). This Figure shows a good agreement between the experimental and the predicted results that have been simulated (each point represents experimental (X-axis) and simulated (Y-axis) values at the same time with the same operating conditions for each point).

The relation between the experimental and simulated results for 2-propylmercaptan are appeared to be straight line with slope to be 1.0 which indicating very good agreement between the measured and predicted results.
Conclusions

1. Oxidative desulphurization process (ODS) appears to be technically and economically valuable for processing ultra-low sulfur fuel from naphtha feedstock. It can be considered as substitute for hydrosulphurization process (HDS). Notably, Oxidation process does not require hydrogen for desulphurization, but instead converts the sulfur compounds present in the naphtha to corresponding sulfide that are then extracted from the naphtha. Prospectively, it is expected that capital cost and operating cost with ODS would be significantly lower than with HDS.

2. It is found that the Non-Linear method, is more accurate based on minimizing the sum of squared error between experimental and predicted results with average absolute error less that 5% among all the results at various operating conditions (LHSV, temperature and initial concentration of inlet sulfur of 2-proplymercaptan).

3. It is found that the 2-proplymercaptan conversion increased as liquid hour space velocity (LHSV) decreased. While increasing temperature causes increase in 2-proplymercaptan conversion.

4. It was found that the oxidation reaction of 2-proplymercaptan is $n^{th}$ order with respect to 2-proplymercaptan concentration and 1.14467 order with respect to catalyst, the activation energy has been estimated to be 17.7071 kJ/mole.

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NOMENCLATURES

| Symbol | Definition | Unit |
|--------|------------|------|
| \(N_{(RSH-C3)}\) | Mole flux of 2 – propyl mercaptan in the feed | mole/m²·time |
| \(A_{reactor}\) | Area of the reactor | m² |
| \(r_{reactor}\) | Radius of reactor | m |
| \(Q_{(RSH-C3)}\) | Volumetric flow of liquid phase | Cm³/time |
| \(-R_{RSH-C3}\) | Rate of reaction for oxidation process | Cm² |
| \(V\) | Bed volume of particle catalyst (Co/AC) | Cm³/mole |
| \(C(RSH-C3)\) | Concentration of \(2 - \) propyl mercaptan | Cm³/mole |
| \(C(RSH-C3)\) | Initial concentration (inlet to reactor) | Cm³/mole |
| \(C(RSHf-C3)\) | Final concentration (outlet from reactor) | Cm³/mole |
| \(K_{Hyl}\) | Hydrodynamic reaction rate constant | mole·cm⁻³·sec⁻¹·(time)⁻¹·(conc.)¹⁻ⁿ |
| \(K_{(RSH-C3)}\) | Kinetic rate constant | mole·cm⁻³·sec⁻¹·(time)⁻¹·(conc.)¹⁻ⁿ |
| \(n\) | Order of reaction kinetic | - |
| \(T\) | Temperature | K or °C |
| \(R\) | Gas constant | J·mol⁻¹·K⁻¹·cm³·atm⁻¹ |
| \(EA\) | Activation energy for oxidation reaction | kJ/mol |
| \(A^\circ\) | Frequency or pre – exponential factor | Cm³/g·sec |
| \(t\) | Time | hr, min, sec |
| \(X_{RSH-C3}\) | Conversion | - |
| \(\tau\) | Residence time | hr |
| \(g\) | Acceleration | cm/sec² |
| \(v_{Naphtha}\) | Velocity of the feedstock (Naphtha) | cm/sec |
| \(\rho_{naphtha}\) | Density of naphtha | g/cm³ |
| \(D_t\) | Tube diameter of TBR | cm |
| \(D_p\) | Particle diameter | cm |
| \(D_pe\) | Equivalent particle diameter | cm |
| \(P_c\) | Critical pressure of naphtha | psia |
| \(MW_{naphtha}\) | Molecular weight of naphtha | Ib |
| \(T_c\) | Critical temperature of naphtha | R⁰ |
| \(Z_c\) | Critical compressibility factor | - |
| \(T_r\) | reduced temperature | - |
| ppm | Part per million | - |
| \(MW_{Oxygen}\) | Molecular weight of oxygen | g/mole |
| \(MW_{Naphtha}\) | Molecular weight of naphtha | Ib |
| \(v_{cNaphtha}\) | Critical specific volume of liquid | cm³/mole |
| \(v_{RSH-C3}\) | Molar volume of DBT at n.b. temperature | cm³/mole |
| \(TmABP\) | Mean average boiling point | R |
| \(\rho_{15.6}\) | Density of naphtha at 15.6 °C | g/cm³ |
| \(\tau\) | Mean pore radius | cm |
| \(S_p\) | External surface area of catalyst particle | cm² |
| \(V_g\) | Total pore volume | cm³/g |
| \(\beta_{ki}\) | Knudsen diffusivity factor | cm²/sec |
| \(R_p\) | Radius of particle for catalyst | cm |
| Symbol | Definition | Unit |
|--------|------------|------|
| $D_{el}$ | Effective diffusivity | $\text{cm}^2/\text{sec}$ |
| $S_g$ | Specific surface area of particle catalyst | $\text{cm}^2/\text{g}$ |
| $D_{mi}$ | Molecular diffusivity | $\text{cm}^2/\text{sec}$ |
| $V_P$ | External Volume of catalyst particle (Co/AC) | $\text{cm}^3$ |
| $V_L$ | Molar volume of liquid at its n.b. temperature | $\text{cm}^3/\text{mole}$ |

**GREEK SYMBOLS**

| Symbol | Definition | Unit |
|--------|------------|------|
| $\psi_{\text{Wett.fact.}}$ | External catalyst wetting efficiency | - |
| $\psi_{\text{Eff.fact.}}$ | Effectiveness factor | - |
| $\tau$ | Residence time | hr |
| $\epsilon_{\text{Void}}$ | Bed void fraction | - |
| $\mu_{\text{naphtha}}$ | Dynamic viscosity of liquid phase | $\text{mPas} \cdot \text{sec}$ |
| $\alpha$ | Constant factor | - |
| $\varphi$ | Volume fraction of molecule | - |
| $\Theta$ | Thiele Modulus | - |
| $J$ | Tortuosity factor | - |
| $\epsilon_s$ | Catalyst porosity | - |