The C-Score: A Bayesian Framework to Sharply Improve Proteoform Scoring in High-Throughput Top Down Proteomics

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Abstract: The automated processing of data generated by top down proteomics would benefit from improved scoring for protein identification and characterization of highly related protein forms (proteoforms). Here we propose the “C-score” (short for Characterization Score), a Bayesian approach to the proteoform identification and characterization problem, implemented within a framework to allow the infusion of expert knowledge into generative models that take advantage of known properties of proteins and top down analytical systems (e.g., fragmentation propensities, “off-by-1 Da” discontinuity errors, and intelligent weighting for site-specific modifications). The performance of the scoring system based on the initial generative models was compared to the current probability-based scoring system used within both ProSightPC and ProSightPTM on a manually curated set of 295 human proteoforms. The current implementation of the C-score framework generated a marked improvement over the existing scoring system as measured by the area under the curve on the resulting ROC chart (AUC of 0.99 versus 0.78).

Keywords: top down proteomics, proteoform characterization, Bayesian scoring

Introduction

Top down mass spectrometry describes an analytical process for the identification and characterization of whole proteins. The canonical “top down” experiment consists of a precursor scan to obtain the intact mass of the proteoform(s) under study and a tandem mass spectrum (MS/MS) obtained using ion fragmentation techniques such as ECD, ETD, HCD, CID, or UVPD. The defining characteristic of a top down experiment is that the precursor ion is an intact proteoform, not the typical small peptides (less than 3 kDa) produced from intentional enzymatic digestion prior to mass spectrometry (MS). Thus, the mass of the precursor ion should represent a native proteoform present in the sample, with its fragment ion masses providing extensive characterization and verification of the primary structure. As larger proteins are targeted, experiments tend toward acquisition logic involving spectral averaging for both the precursor and fragment ions to improve the data quality. These combined data are then analyzed to infer the neutral masses of all intact and fragment ion species observed. For proteins analyzed by electrospray ionization, this Analysis to Infer Mass (AIM) uses either isotopic spacings for direct charge state assignment and/or deconvolution of protein charge states.

Historically, top down mass spectrometry has targeted the in-depth characterization of a small number of proteoforms, however, the past 5 years has seen a gradual transition to “top down proteomics” where thousands of proteoforms from dozens of LC−MS/MS runs are analyzed. While the number of proteins able to be identified has risen into the thousands, the extent of characterization of each individual proteoform varies and currently there is no scoring framework that captures this aspect of top down proteomics. In certain cases, a protein (arising from a specific gene) may be identified confidently with no inference problem whatsoever, yet may be only partially characterized as shown in Figure 1. In Figure 1B, two “equivalent” proteoforms, one with a post-translational modification (PTM) in the first position and the other with the PTM in the second, will each have the same number of matching fragment ions. Scoring systems based only on matching ions will report equal scores for these two proteoforms. This example illustrates how a proteoform can be clearly identified (i.e., the evidence supporting the identification of either of the two positional isomers is strong), yet not fully characterized. This problem of PTM site

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Figure 1. Incomplete fragmentation may or may not lead to partial characterization of a protein molecule. In panel (A), the matched fragment ions uniquely determine the location of the post-translational modifications (PTMs). In panel (B), incomplete fragmentation in the middle of the protein backbone does not yield a definitive PTM localization. In this particular example, the PTM could be located at either of two amino acids, resulting in an identified, but partially characterized proteoform. The C-score framework was developed to handle such cases, routinely encountered in top down proteomics. N-terminal fragment ions are colored red, while C-terminal fragment ions are shown in blue. The numbers below the fragment ions indicate how many PTMs are reported on by each ion.

localization is encountered in bottom up, and has been dealt with in various ways.16−18 In targeted top down MS generating just a few spectra, manual reanalysis of data, or curation of the primary literature, can be used to select one protein form over another highly related one. In such cases, expert decisions are made to distinguish proteoforms with similar primary structures taking into account cleavage propensity of pairs of amino acids, complementary ion pairs, sequence tags, and mass errors of precursor and fragment ions.

With the shift to high-throughput, fully automated data collection, we now seek a framework for scoring of protein identification and proteoform characterization that builds in domain knowledge to achieve the quality of manual analysis without requiring it. All of the mathematical symbols used below are aggregated into Table 1. Fundamentally, the problem of identifying which proteoform is most consistent with an experiment combines both aspects of protein identification (which gene) and characterization (which proteoform). In practice, the problem is one of testing a series of hypotheses about which proteoform was present in the mass spectrometer, and then picking the “best” hypothesis from the list. Each candidate proteoform (not simply its protein sequence) constitutes a hypothesis, but since candidate proteoforms do not represent all possible hypotheses to be tested, a scoring system must allow for the possibility that the best scoring proteoform is near the correct answer, but not exactly correct. Further, it is frequently the case that the observed data cannot conclusively differentiate between two or more related proteoforms (as in Figure 1B), or the case where multiple proteoforms were actually fragmented together. Typically, the way a proteoform score is used experimentally is not too dissimilar the use of scores in annotating novel nucleotide sequences with BLAST. For a given search, a minimum cutoff threshold is picked by the operator (a priori), and for each query the answer accepted as correct must be both the highest scoring result and greater than the cutoff threshold.

The problem of inferring which proteoform, from the articulated “prior” list of proteoforms in a database, was observed within the mass spectrometer is well-suited to a Bayesian approach (Figure 2). In this case, Bayes law can be rearticulated as follows:

\[
\Pr(\text{Proteoform} | \text{Data}_{\text{MS/MS}}) = \frac{\Pr(\text{Proteoform}) \times \Pr(\text{Data}_{\text{MS/MS}} | \text{Proteoform})}{\Pr(\text{Data}_{\text{MS/MS}})}
\]

where (1) \(\Pr(\text{Proteoform} | \text{Data}_{\text{MS/MS}})\) is read as the probability of the ith Proteoform given the MS/MS data, and is known as the posterior probability of proteoform i given the observed data; (2) \(\Pr(\text{Proteoform})\) is known as the prior probability of proteoform i; (3) \(\Pr(\text{Data}_{\text{MS/MS}} | \text{Proteoform})\) is read as the probability of the data given proteoform i, and is known as the likelihood of the data given proteoform i; (4) \(\Pr(\text{Data}_{\text{MS/MS}})\) is known as the probability of the data. By convention, this can be taken as the sum of all prior probabilities multiplied by their

| symbol | meaning |
|--------|---------|
| \(\Pr(\text{Proteoform} | \text{Data}_{\text{MS/MS}})\) | Probability of the ith proteoform given the MS/MS data, and is known as the posterior probability of proteoform i |
| \(\Pr(\text{Proteoform})\) | The prior probability of proteoform i |
| \(\Pr(\text{Data}_{\text{MS/MS}} | \text{Proteoform})\) | The probability of the data given proteoform i, and is known as the likelihood of the data given proteoform i |
| \(\Pr(\text{Data}_{\text{MS/MS}})\) | The probability of the data. By convention, this can be taken as the sum of all prior probabilities multiplied by their likelihoods across all hypotheses. |
| \(M_{o}\) | Observed precursor mass |
| \(m_{i}\) | Mass of the ith of n observed fragment ions |
| \(\{m_{i}\}_{i=1}^{n}\) | The set of all n observed fragment ions |
| \(\phi_{k}\) | The qth of k candidate proteoforms in the database |
| \(\Pr(\phi_{k})\) | The prior probability of \(\phi_{k}\) |
| \(\Pr(M_{o}, m_{i} | \phi_{k})\) | The likelihood of proteoform \(\phi_{k}\) given the observed precursor mass and fragment masses. |
| \(k\) | The number of proteoforms potentially explaining the observed masses. |
| \(\Pi_{k} \times \Pr(m_{i} | \phi_{k})\) | The product of the individual likelihoods for each observed fragment ion, given the qth candidate proteoform. |
| \(M_{0}\) | The theoretical intact mass of candidate proteoform j |
| \(\delta_{a}\) | The difference between the observed and a candidate mass. Either at the MS1 or MS2 level. |
| \(\omega_{k}\) | A weight representing the propensities for the ith pair of amino acids to cleave during fragmentation. It is taken as proportional to the product of the cleavage frequencies for both flanking amino acids. |
| \(\omega_{k,\text{prior}}\) | The weight assigned to observed MS2 masses that do not match a theoretical MS2 mass for a given candidate proteoform. |
| \(t_{i}\) | The total area under the MS2 generative model. An intermediate value used to find probabilities. |
Bayesian law provides a useful foundation for building these models. In practice, it is not required that the list of candidate proteoforms be explicitly articulated prior to the analysis. It is sufficient that all candidate forms can be calculated for an explicitly stated set. For example, listing base protein sequences and the PTMs to be considered on these sequences defines a list of proteoforms, even if the list is never explicitly written.

The posterior probability to be the fraction of the total of the likelihoods across all hypotheses. Notice that this term scales the posterior probability to be the fraction of the total of the numerators over all proteoforms interrogated. Thus, a multiple testing correction across the database search is integral in this approach. This differs from controlling for the overall false discovery rate of an experiment which can, for example, be handled posthoc with a search against a scrambled sequence database in a manner analogous to that used in earlier work.  

To be precise, we will define the following variables to restate Bayes law from eq 1. Let \( M_\text{O} \) = observed precursor mass, \( m_i \) = mass of the \( i \)-th of \( n \) observed fragment ions, so \( \{m_i\}_{i=1}^n \) is the set of all \( n \) observed fragment ions, and \( \phi_i \) = the \( q \)-th of \( k \) candidate proteoforms in the database. The posterior probability of hypothesis \( \phi_q \) as per eq 1, can be restated as

\[
Pr(\phi_q|M_\text{O}, \{m_i\}) = \frac{Pr(\phi_q) Pr(M_\text{O}, \{m_i\}|\phi_q)}{Pr(M_\text{O}, \{m_i\})}
\]

where \( Pr(\phi_q) \) is the "prior" term and \( Pr(M_\text{O}, \{m_i\}|\phi_q) \) is the "likelihood" term.

Since the probability of the data is, by convention, known, two values are needed to calculate the posterior probability for each hypothesis: the prior probability and the likelihood for the data. In many applications, the prior probabilities can be taken to be "all hypotheses are equally probable" (i.e., uniform prior probabilities). If there are "\( k \)" competing hypotheses, that is, "\( k \)" proteoforms in the candidate list, then each proteoform has a prior probability of \( 1/k \), but this does not need to be the case. It is possible that one would want to assign proteoforms of proteins that contain experimentally demonstrated PTMs (or transcripts informed by RNA-Seq) higher prior probabilities than proteoforms that contain chemically possible, but otherwise rarely observed modifications. For example, if there are two proteoforms that differ only in the location of a PTM such as in Figure 1B, and one of the PTMs was known to occur, while the other had never been reported, and the set of observed fragment ions failed to differentiate the two forms, then the known form should be considered the most probable form to have been observed. This degree of differentiation can be achieved with such a scoring system by first setting and then improving the prior probabilities with continued experimentation. Prior probabilities are, by definition, based on information known prior to data collection and are in practice always somewhat arbitrary in their determination. In sharp contrast, the likelihood of the data given the proteoform is calculated under an explicit mathematical model of the processes used to generate top down MS data; calculation of this likelihood requires generative models.

Generative models “generate” the probability of the observed data, given the proteoform in question. Therefore, they take as input the proteoform, and as much knowledge of the measurement process as can be encoded in the model-creation process. For example, a generative model could include the propensity of individual pairs of amino acids to dissociate during fragmentation (e.g., X-P cleavage in ECD and ETD is not possible, yet DP bonds are preferentially cleaved in threshold dissociation), or the model could include a function for the difference between the observed and theoretical intact mass. The more knowledge of the measurement process the generative model includes, the better, but since the task is to rank order the list of candidate proteoforms (Figure 2), some details can be safely excluded from the generative model if they do not shift the proteoform rankings.

This Bayesian approach offers many advantages. First, it logically follows what many are already doing in the field. For example, during manual data interrogation of an error-tolerant, top down search result, many researchers prefer the observed intact mass to match the theoretical, but allow for the possibility that the masses may not match because the best proteoform in the database is not the correct one. Any scoring system that does not include the closeness of the observed MS1 to the theoretical MS1 is ignoring a valuable observation. Next, this Bayesian framework explicitly states the process in the form of two generative models; one for the precursor mass, and the other for the fragment ion masses. Since the models are clearly articulated, they can be defended, rejected, or modified based on community discourse. In practice, this means that the process model can be modified and updated to reflect new understanding of the measurement process, or to reflect changes to the process used. For example, an automated data analysis system can use the same scoring mechanism, but employ different parameter sets that reflect experimental differences. Experiments that use CID or HCD will employ different parameter sets in the generative models used for scoring than the same top down experiment employing ECD/ETD or UVPD for protein ion fragmentation.

It should be noted that the calculation of scores in this system differs from Bayesian approaches commonly seen in biological sequence analysis. In those applications, the generative models usually have unknown parameters that
need to be estimated from the sequence data, which is usually taken as being perfectly known. The application here is more like that of Edwards where the process is considered known. As will be seen, our generative models have no unknown parameters; instead all values are taken from our knowledge of mass spectrometry, or from prior studies that focused on determining the needed value. Thus, instead of inferring values from the data collected for the study in question, we have a framework for applying knowledge gained in analytic chemistry to the problem of protein inference.

Currently, ProSightPC and ProSight PTM report an AUC of 0.85 versus 0.80 in ProSightPC.23 The ProSight PTM expectation value used within ProSightPTM and scoring, and compare one set of generative models to the other.

First the magnitude of it impossible to directly compare scores between separate models. The observed number of MS2 fragment ions lower the calculated value of the MS2 fragment ion masses, that is, masses of the products resulting from fragmentation of the proteoform. Also required is a database of possible proteoforms, each of which serves as a hypothesis that could potentially explain the observed MS/MS data. The database of possible proteoforms was generated by combinatorial expansion of all potential proteoforms using the known modification information in the UniProt Knowledgebase.25–28

Derivation of the Likelihood
Since the observed data MO and each fragment ion, mi, are independently conditioned on qφ, we could take

\[
\Pr(M_O, \{m_i\}|q_φ) = \Pr(M_O|q_φ) \prod_{i=1}^{n} \Pr(m_i|q_φ)
\]

Unfortunately, this approach suffers from two limitations. First the magnitude of \( \prod_{i=1}^{n} \Pr(m_i|q_φ) \) scales with n. Larger lists of MS2 fragment ions lower the calculated value of the MS2 likelihood, relative to lists with few fragment ions, which makes it impossible to directly compare scores between separate queries with differing numbers of MS2 fragment ions. This can be mitigated by weighting by the geometric mean of the number of MS2 fragment ions; 1/n. Second, this approach weights the MS1 data as simply a single additional matching fragment ion. To avoid this, we introduce two scaling functions, f and g, to map the ranges of the individual generative model to a normalized range;

\[
\Pr(M_O, \{m_i\}|q_φ) = f(\Pr(M_O|q_φ)) g(\prod_{i=1}^{n} \Pr(m_i|q_φ)^{1/n})
\]

For the precursor generative model, the function \( f ) is simply the identity function. For the fragment ion generative model, we define \( g \) by its logarithm base, which is simply a linear function on the logarithm base 10 of the fragment probability; \( g \) sets the logarithm base 10 of the minimum possible fragment probability to the logarithm base 10 of the minimum possible precursor probability and likewise for the maxima. If \( \min_q \) is the minimum precursor probability, \( \max_q \) is the maximum precursor probability, \( \min_q \) is the minimum fragment probability, and \( \max_q \) is the maximum fragment probability, then

\[
\log_{10} g((\prod_{i=1}^{n} \Pr(m_i|q_φ)^{1/n})
\]

\[
= (\log_{10} \max_q - \log_{10} \min_q) \times (\log_{10}(\prod_{i=1}^{n} \Pr(m_i|q_φ)^{1/n})
\]

\[
- \log_{10} \min_q + \log_{10} \max_q
\]

Derivation of the Posterior Probability
Under an assumption of uniform prior, and given the likelihood functions from above, we have

\[
\Pr(q_f|M_O, \{m_i\}) = \frac{\Pr(q_f|M_O, \{m_i\}|q_φ) \Pr(M_O, \{m_i\}|q_φ)}{\sum_f \Pr(q_f|M_O, \{m_i\}|q_φ) \Pr(M_O, \{m_i\}|q_φ)}
\]

\[
\Pr(q_f|M_O, \{m_i\}) = \frac{f(\Pr(M_O|q_φ)) g((\prod_{i=1}^{n} \Pr(m_i|q_φ)^{1/n})}{\sum_f f(\Pr(M_O|q_φ)) g((\prod_{i=1}^{n} \Pr(m_i|q_φ))}
\]

Equation 2 therefore reduces the posterior probability of a hypothesis to the data likelihood computation, with a normalization factor equal to the sum of the likelihoods under all possible hypotheses. All that is needed now to calculate posterior probabilities are the generative models. Since we have assumed that the given database of proteoforms is an exhaustive set of hypotheses, these generative models must allow for the possibility of observing related proteoforms that are not present in the database.

Generative Models
The C-score system requires two generative models; one for the precursor mass MO and the other for the set of observed fragment ion masses, \( \{m_i\} \). These models fully prescribe how to compute the likelihood terms on the right-hand side of eq 2. Note that the particular form of eq 2 implies that all the likelihood (probability) terms need only be computed up to a constant factor. This constant factor cancels between the numerator and denominator of the RHS of eq 2.

The probability \( \Pr(M_2|q_φ) \) of an arbitrary protein sequence \( q_φ \) (of theoretical mass \( M_2 \)) producing the observed precursor mass \( M_O \) can be modeled as a function of \( δ_{qφ} \), the difference between the \( M_O \) and \( M_2 \). We create the probability distribution \( \Pr(M_2|q_φ) \) such that masses within \( δ_{qφ} \) of \( M_2 \) have the highest probability, and this probability reduces as a truncated Gaussian function with \( μ = 1 \), \( σ = 30 \) Da, and a minimum value of \( 1 \times 10^{-300} \). Notice that we only need to specify \( \Pr(M_2|q_φ) \) to a constant factor (i.e., we only need to specify a non-negative function \( f(M_2, q_φ) \) proportional to the probability), and the normalization factor \( \int_{\text{max}_M}^{\text{max}_M} f(M_2, q_φ)dM_O \) that converts it to a probability density function is assumed implicitly.
To specify the probability distribution $Pr(m|\phi_i)$, we need an MS2 generative model based on our knowledge of the measurement process during tandem mass spectrometry. We note that each fragmentation event involves cleavage of the intact proteoform at one bond on the protein backbone, resulting in exactly two fragments (although both may not be observed in the spectrometer). The fragmentation propensity depends on the pair of adjacent amino acids flanking the cleavage site. The generative model we choose is based on this observation, and uses the following basic ideas:

1. Each theoretically possible fragment ion mass defines a region of width $2\delta_m$ ($m - \delta_m, m + \delta_m$) called a permissible region. An observed mass $m_i$ within a permissible region has a probability proportional to the cleavage propensity of gas phase protein ions at that permissible region.
2. An observed fragment ion mass $m_i$, outside of any permissible region has a small, constant probability.

These ideas are captured in the probability distribution function of Figure 3. In principal, for any given $\phi_i$, the probability distribution $Pr(m|\phi_i)$ is constructed by assigning a height to every point in the range $(0, M_i)$, where $M_i$ is the theoretical precursor mass. In practice, MS2 mass lists can contain unexpected ions with mass values greater than $M_i$, and so an arbitrarily large mass of 4 million Daltons is taken in place of $M_i$. (The value of 4 million Daltons was selected as it is safely above the mass of the largest protein known, titin at 3.9 MDa, and allows for a modified form of titin to be present. In practice, this value is effectively infinity.) The assigned heights across the entire range are divided by the total area under the curve, thus defining a probability density function. The heights are assigned as follows:

- Step 1: Determine all theoretical fragment ions that $\phi_i$ can give rise to, noting their mass and the N- and C-terminal flanking amino acids at each cleavage site.
- Step 2: For each theoretical fragment ion, calculate a weight, $\omega_i$, proportional to the product of the cleavage frequencies for both flanking amino acids as previously determined for the appropriate fragmentation method. Thus, if $\alpha$ and $\beta$ are the two flanking amino acids, and $f_\alpha$ and $f_\beta$ are their respective cleavage frequencies, we set $\omega = f_\alpha f_\beta$. The permissible region associated with a theoretical fragment ion mass, $m_i$, is assigned a consistent height equal to the weight $\omega$ computed for the corresponding theoretical fragment ion.
- Step 3: Any point in the range $(0, M_i)$ but outside of all permissible regions is assigned a height of $\omega_{\text{noise}}$, which is a constant. This term represents spectral noise.

We noted above that the probability density function is obtained by dividing the above-mentioned “height” function by the sum of the area under the curve, which is different for different $\phi_i$. This total area, denoted by $t_\phi$, is computed as follows: the $k$th permissible region has a height equal to $\omega_k$ and a width equal to $2\delta_m$. Regions outside of permissible regions have a height of $\omega_{\text{noise}}$ and a total width of $P = 2(len - 1)\delta_m$, where $len$ is the length of the protein sequence. Thus, $t_\phi = \omega_{\text{noise}}(P - 2(len - 1)\delta_m) + \Sigma 2\delta_m\omega_k$.

The resulting probability density function is

$$Pr(m|\phi) = \begin{cases} \frac{\alpha_k}{t_\phi} & \text{for } m_i \text{ in a permissible region with weight } \omega_k, \\ \frac{\omega_{\text{noise}}}{t_\phi} & \text{for } m_i < P, \text{ but not in a permissible region,} \\ 0 & \text{otherwise} \end{cases} \tag{3}$$

The expressions on the right-hand side specify a probability density while the expression on the left-hand side is a probability mass, which, strictly speaking, should be equated to the probability density over a very small mass interval, $\delta$. However, such a correction can be safely ignored here because the probability mass $Pr(m_i|\phi)$ is used only in the context of eq 2, with equal powers of $\delta$ in numerator and denominator.

Using eqs 2 and 3, it is now possible to calculate a posterior probability $Pr(\phi_i|M_m(m_i))$ for every sequence $\phi_i$ in the database. This posterior probability is proportional to the likelihood $Pr(M_m(m_i)|\phi_i)$ since we assume uniform priors (eq 2). Therefore, our search for the maximum a posteriori hypothesis $\phi_i$ is equivalent to a maximum likelihood estimation (MLE) search, that is, we report the $\phi_i$ that maximizes $Pr(M_m(m_i)|\phi_i)$.

**The Characterization Score, or C-Score**

We report the best hypothesis $\phi_i$ along with its “Phred-like” characterization score,$^{31}$ which can be written as $C = -10\log_{10}(1 - Pr(\phi_i|M_m(m_i)))$. This final C-score transformation scales the posterior probability of $\phi_i$ to the familiar range used in many other bioinformatic applications. C-scores span the standard Phred-like score range of 0 to >500. Practical ranges of the C-score are evaluated with specific examples and reported in the main text below. Therefore, a C-score of 40 is sufficient to judge a proteoform as extensively or fully characterized, while proteoforms with C-scores between 3 and 40 are identified, but only partially characterized. A C-score below 3.

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**Figure 3.** MS2 generative model for fragment ions observed in tandem mass spectrometry (MS/MS). For instruments capable of MS/MS with accurate mass, thin (e.g., low part-per-million wide) permissible regions occur with a search-defined width around each theoretical fragment ion mass. The heights of these regions are scaled by the propensity of the cleavage events required to form the theoretical ion. Different fragmentation methods require different weights, for example ECD has different fragmentation propensities than CID. A very low probability, the weight for chemical or electronic noise, is assigned to any observed mass that does not match one of the theoretical masses.
indicates insufficient evidence for either identification or characterization. Note also that since the C-score represents a nonlinear transformation of the posterior probability, which is itself normalized by Pr(Data|MS/MS), there is a functional relationship between the highest score in a search, and the second highest score (Supporting Information Figure 1).

**Approach to Comparing Scores**

The typical usage of a score such as the C-score is in high throughput data processing. An operator picks a threshold level of the score and then asserts that any query scoring above the threshold identifies the target data. This is done routinely in annotating DNA sequences with tools such as BLAST. To test the utility of a new scoring model, a set of data where the correct answer can be considered known is needed; this forms the ‘ground truth’ of the analysis. When the new scoring system gives the known true answer both as the highest score, and the scoring above the operator-defined threshold, the system is said to have delivered a “true positive”. Likewise, when the best proteoform scoring above threshold is not the known correct answer, it is scored as a false positive, and so on for both true and false negatives. Sensitivity is the proportion of positives which are actually classified as such for a given threshold. Likewise, specificity is the proportion of negatives that are correctly identified as such.

For any given arbitrary threshold of a score, a specificity and sensitivity can be calculated from a known data set. By iterating over a number of thresholds, and plotting the resulting sensitivity against its corresponding specificity (or by convention, against 1-specificity) a “receiver operating characteristic” curve is generated. This curve is known to be indicative of the utility of the classifier. By repeating this iterative analysis of with multiple scoring systems, the relative utility of the systems can be directly compared. So, to compare the new C-score with the existing ProSight E-value, test input data sets with known correct answers are needed. These data sets are searched against the appropriate proteoform database and, for each proteoform returned, the E-value and C-score is calculated. Next, an arbitrary list of threshold values is generated for each score, and for each threshold value in this list, a list of identified proteoforms is generated. The identified proteoform is taken as the form that is both above the threshold score, and to be the highest scoring proteoform. It is therefore possible for a search not to return a proteoform, if no proteoform scores above the cutoff threshold. When searching a test data set with known correct answers, it is possible to classify the search results as either a true positive, true negative, false positive, or false negative. From these classifications, specificity and sensitivity is calculated for each threshold level. These specificity and sensitivity couplets then become points on the ROC chart curve for a given score.

**Test Data Sets**

**Data Collection.** The human data files used in this analysis were acquired in the course other studies published previously. Briefly, mitochondrial membrane proteins were isolated from HeLa S3 cells and separated using a GELFrEE 8100 Fractionation system (Expedeon) as described previously. For the analysis at hand, 295 top down experiments from a nanoLC-Velos Orbitrap Elite MS analysis of a GELFrEE fraction containing ~15–20 kDa proteins were selected for intensive manual interrogation to provide a set of highly curated “known positives” to test parameter sets within the generative models used in development of the C-score framework. *Pseudomonas aeruginosa* were grown on rich media to mid-log phase, were isolated by centrifugation, lysed, separated with GELFrEE, and analyzed with mass spectrometry using the methods referenced above. For the secondary data set, 136 top down experiments were curated to select true-positives for analysis.

**Manual Data Analysis.** A descriptive analysis of intact and tandem mass spectral data was performed using RawMeat 2.1 (http://vastsci.com/rawmeat/, VAST Scientific). Using these data, related MS2 scans were merged and individual ProSight Upload Format (PUF) files were created for each data set. A combination of QualBrowser and ProSightPC 3.0 (both Thermofisher, San Jose, CA) was used, and all potential precursors predicted to have been in the MS1 Isolation Window were added as potential proteoforms for the experiments. Both MS1 and MS2 data were deisotoped using the Xtract algorithm embedded within ProSightPC 3.0, generating 623 single experiment PUF files. Each experiment was manually searched against “homo_sapiens_2012_02_top_down_simple” (containing 460 000 forms) and “homo_sapiens_2012_02_top_down_complex” (containing just over 10 million forms) which are ProSight Warehouses (.pwf files) for human proteins built against UniProt release 2012_02, available for download (ftp://prosightftp:gsX1gON@prosightpc.northwestern.edu/2012_02/Eukaryotes/Homo%20sapiens/). Experiments with single “correct” proteoforms were selected and verified by at least two group members trained in top down proteomics data analysis, to be considered as true answers, and while subjective each met the following two criteria: the most abundant fragment ions must be accounted for, and the intact mass difference between theoretical and experimental must be small (<10 ppm) or must be explainable (±1 Da errors from deisotoping, a previously unknown or unannotated post-translational modification, oxidation, etc.). This will typically involve the assignment of >50% of fragment ions appearing at a signal-to-noise of 10:1 or higher. However, we note that both experimental conditions (e.g., overfragmentation, generating internal ions) and the selection of data processing parameters will affect the quality of data and thus the fraction of ions matched for each experiment.

If evidence was not sufficient to uniquely identify one proteoform for an experiment (arising either from poor data quality or from multiple proteins being fragmented simultaneously), the experiment was excluded from further study here. Using these heuristics, 295 PUF files where only one proteoform was present were selected for use here. These files are described in Supporting Information Table 1 and provided in Supporting Information Data Set 1.

**Implementation**

To facilitate a comparison of C-scores and E-values, a custom C# .NET 4.5 console application was developed. This application takes, as input, a collection of PUF files, the list of manually validated correct answers, and the C-score version number (with a specific parameter set) to use. The C-score version allows various iterations of generative models to be tested against the E-value and each other. The output from the application is an Excel spreadsheet containing a correct score and actual score for both the E-value and the C-score. During execution, this application runs ProSightPC27 Absolute Mass and BioMarker searches on each PUF file to compile actual search scores. The correct scores are then calculated using the
Comparison

To compare the E-value to the C-score, we chose as our first input a set of 295 PUF files (described above) and a C-score version of 1.0. The list of correct proteoforms for each of the 295 targets was provided as a CSV file. The custom console application was then used to generate an Excel spreadsheet that was further analyzed. Two ROC curves (one for each score) were plotted on the same chart by checking, for each target, whether the top scoring proteoform was the correct proteoform (Figure 4). Subsequently, additional ROC curves were generated, where a target was counted as incorrect if the correct proteoform merely tied for the best score, but other proteoforms also shared the same score value. We also calculated the area under each curve as a quantitative measure of difference. Two additional ROC curves where generated as before but the correct answer would only be considered a true positive if it uniquely had the best score. Thus, for these curves, if the correct proteoform failed to out-score all other proteoforms in the database it was not considered a true positive. This process was repeated for 136 proteoforms from Pseudomonas aeruginosa (data are provided in Supporting Information Data Set 2).

RESULTS AND DISCUSSION

The C-score was substantially better than the E-value at identifying and characterizing the correct proteoform from the data set of 295 human test cases, as well as the 136 Pseudomonas test cases. Figure 4 shows a receiver operating characteristic (ROC) curve for both scores on the human data, and the area under the curve for the C-score was 0.99 compared to only 0.78 for the E-value. For the Pseudomonas test cases, the C-score also outperformed the E-value with AUCs of 0.85 to 0.80, respectively.
Clearly, the C-score (with the v1.0 parameter set) dominates the E-value for all levels of specificity and sensitivity. Since the E-value is simply a nonlinear transformation of the number of matching fragment ions, it seems reasonable to assert that this improvement comes from the new score’s ability to include additional factors such as known fragmentation propensities and MS1 mass differences both of which are known to be relevant in characterizing proteoforms. These and other such factors are not considered by the current E-value, nor is the score easily extended to consider such factors.

When the data are sufficient to completely characterize a proteoform, the C-score is often well above 40, indicating hyperconfidence in the characterization power of the underlying data (Figure 5A). However, a major limitation of the E-value occurs when many proteoforms share the same (seemingly confident) score. This can be seen in Figure 4 as the vertical distance between the two E-value lines in the specificity range of 0.8−1.0 (FPR 0.0−0.2). Figure 5B and C shows two example cases where there is equal evidence for two distinct proteoforms, one with an N-terminal acetylation and the other with the acetylation localized to K7. In this example, these two proteoforms share a confident E-value of 7 × 10^-60; however, their C-scores are tied, yet at a much less confident value of 3. Using the data from these two manually annotated sample sets, and with the understanding of the C-score model, we assert three operating ranges for the C-score: C-score > 40 → proteoform is both identified and fully characterized; 3 ≤ C-score ≤ 40 → proteoform is identified, but only partially characterized; C-score < 3 → proteoform is neither identified nor characterized.

To achieve separation between the two proteoforms in Figure 5B and C, future iterations of the C-score will allow for differential probabilities for N-terminal acetylation and internal acetylation. It has been reported that over 80% of all human proteins are constitutively N-terminally acetylated,35 so one may posit that, in the absence of evidence to the contrary, N-terminal acetylation is more likely than internal acetylation. The C-score model can incorporate this bias and many similar issues that provide biochemical and biological context. To achieve even more specificity and sensitivity in the C-score framework, one may use a proteomic database, such as GPMdb, to use peptide-level information linked to the specific gene product to inform these differential probabilities in top down proteomics experiments.36 In the case of UniProt entry P61604, GPMdb reports that N-terminal acetylation was observed in 69/69 studies, making the proteoform reported in Figure 5B a much more likely than the proteoform reported in Figure 5C.

The characterization of high-throughput LC−MS/MS experiments, where hundreds of MS/MS targets are automatically generated for each LC run, forms the foundation of high throughput top down proteomics. Our probabilistic formulation leverages the knowledge of fragmentation propensities and may be further extended to incorporate other types of prior information to improve the scoring (vide supra). To characterize unknown PTMs (e.g., a previously unknown methylation), we can extend our C-score model to give a higher probability to common PTM mass shifts (i.e., 42.0105 Da for acetylation, 79.966 Da for phosphorylation, etc.), thereby boosting the data likelihood. This will be particularly useful in complex eukaryotic proteomes where the inclusion of all theoretically possible proteoforms in the database (even at search run time) is computationally prohibitive.

This framework provides a great deal of flexibility for having an appropriate scoring systems for a given experimental procedure. Our current assumption of uniform priors on candidate proteins makes our procedure a maximum likelihood (ML) inference, but the framework can be readily extended to allow for nonuniform priors without additional overhead. Nonuniform priors may be useful when researchers have a priori belief that some protein forms (e.g., particular combinations of PTMs or splice variant) are more likely to be present in the sample (e.g., from RNA-seq data). Further, the score remains robust when used with instruments with decreasing mass accuracy. Supporting Information Figure 2 shows the ROC chart resulting from rerunning the analysis on the human test data set with increasing mass tolerances. As tolerance increases, the discriminative power of the score decreases as more fragment ions will match by chance.

## CONCLUSION

In sum, we have shown a promising scoring system for protein identification and proteoform scoring to better capture the information content in high-resolution top down proteomics. The C-score model lays forth a path to increase the sophistication of protein identification and characterization platforms to extract maximum value from MS-based proteomics in automated fashion. The conceptual and demonstrable advances outlined above provide a deterministic process to advance the utility of proteomics for nonexperts. We strive to enable both proteomics experts as well as “non-bioinformatics/nongenomics” to advance protein-based science based on proper description of the fully articulated primary structure for whole proteomes. When coupled with high value experimentation, we posit that the faithful and more efficient conversion of data streams into knowledge will significantly advance major breakthroughs in mechanistic biology and on the front lines of disease research including improved discovery and validation of protein-based biomarkers.

## ASSOCIATED CONTENT

S Supporting Information

Supplementary Table S1, Supplementary Figures 1 and 2, zipped XML files containing precursor and fragment ions for all 295 human top down experiments used in this study (Supplementary Data Set 1), and zipped XML files containing precursor and fragment ions for all 136 Pseudomonas aeruginosa top down experiments used in this study (Supplementary Data Set 2). This material is available free of charge via the Internet at http://pubs.acs.org.

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Notes

Any opinions, findings, and conclusions or recommendations expressed in this material are those of the authors and do not necessarily reflect the views of the National Science Foundation, the National Institutes of Health, the National Center for Genome Analysis Support, Northwestern University, or Indiana University.
The authors declare the following competing financial interest(s): Several of the authors are also developers on ProSightPC, a piece of commercial software mentioned in the manuscript.

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**ABBREVIATIONS**

CID, collisionally induced dissociation; HCD, higher energy collisional dissociation; ETD, electron transfer dissociation; AUC, area under the curve; ROC, receiver-operating characteristic; RHS, right-hand side (of the equation); Pr, probability; PUF, ProSight Upload Format; CSV, comma separated values; FPR, false positive rate; TPR, true positive rate; ML, maximum likelihood; MS, mass spectrometry; MS1, intact/precursor scan; MS2 (or MS/MS), tandem mass spectrometry scan, fragmentation; PTM, post-translational modification; UVPD, ultraviolet photodissociation.

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