Nanostructured (NS) metals feature high strength [1–8], but typically have low ductility [1,9–12]. When stretched alone, NS metals intrinsically tend to develop shear bands soon after yielding, which propagate quickly through the cross-section [9–12], ending uniform elongation. This is because NS metals have low strain hardening capability [1,9–12]. Strategies for improving ductility [9–19] are mostly related to the recovery of intra-granular dislocation-mediated plasticity [5,10–14], which is, however, limited by either the small grain sizes or initial near-saturation dislocation density [2,3,9,10], both of which limit dislocation accumulation capability during tensile testing [9–11].

Ductility is generally defined as uniform elongation in the specimen gage length during tensile testing [20]. It can be determined by the Considère criterion [21], \((d\sigma/d\varepsilon)/\sigma \geq 1\), where \(\sigma\) is true stress and \(\varepsilon\) true strain, or by the Hart’s criterion [20], \((d\sigma/d\varepsilon)/\sigma + m \geq 1\), where \(m\) is the strain rate sensitivity. Neither criterion literally specifies whether homogeneous strain in the gage section is a must for ductility, which raises a question: is it possible to maintain high ductility if strain is not uniform?

We investigated this issue using a gradient structured (GS) interstitial-free (IF) steel, consisting of NS surface layers with a continuous increase in grain sizes along the depth to the central coarse-grained (CG) layer [11,12]. It is found that shear bands were formed in the NS layers at a very early stage during tensile testing, as NS metals typically do. Unexpectedly, the shear bands became stabilized due to strain gradient and propagated slowly along the gage length to become a localized strain zone (LSZ), which produced synergistic strain hardening to help with retaining ductility. In other words, the shear bands helped with retaining ductility, contrary to our conventional understanding of strain localization [22–24].
CG IF steel plate of 1 mm thick with a mean grain size of 26 μm was used as the initial material. Gradient structure (GS) was prepared using surface mechanical attrition treatment (SMAT) technique [25]. The NS layer is ~40 μm thick, with a mean grain size of 200 nm.

The tensile samples were dog-bone shaped with the gauge section of 1 mm × 2 mm × 10 mm. Uniaxial tensile tests were conducted at a strain rate (ε˙) of 8 × 10⁻⁴ s⁻¹ under room temperature. Digital image correlation (DIC) imaging was performed on the top NS surface layer (see Supplementary Material). Microstructures, texture, and Vickers micro-hardness (HV) were characterized on samples subjected to various tensile strains. HV was measured with load of 25 g and dwell period of 15 s on NS surface after grinding off surface roughness by ~10 μm deep. Focused ion beam was used to cut the cross-sectional transmission electron microscopy (TEM) samples precisely in the shear band and LSZ in the NS layer at varying tensile strains according to the DIC image.

Figure 1(a) shows the microstructure of the central CG layer with an average grain size of 26 μm, and Figure 1(b) shows the nanostructure in the NS surface layer at ~40 μm depth, which reveals entangled dislocations in grain interiors and the average grain size is 200 nm, typical of severely deformed metals [3,4,26]. The corresponding HV gradient is visible from the surface to the center (Figure 1(c)).

Figure 2(a) shows the true stress–strain (σ–ε) curves of GS and CG samples. The GS sample shows uniform elongation (EU) of 20.6%, which retained about 80% of that (26%) of the CG sample, while doubled yield strength. Figure 2(b) shows a set of typical contour maps showing longitudinal (axial) strain (εL, %) distribution at varying applied tensile strains (εapp, %). At εapp = 1%, two shear bands crossing each other were formed in the upper part of the sample. The shear bands are measured at ~45° to tensile axis, with the orientation of maximum resolved shear stress. Thus, the plastic response in NS layer begins with the nucleation of shear bands. These two shear bands propagated downward with increasing εapp along the gauge length and continually broadens to form an LSZ, see maps with increasing εapp from 2.7% to 15.8% until necking at εapp = 20.6% (EU) (Figure 2(a)). A weaker LSZ is also visible in the lower part but fail to propagate much. In every sample tested, there is only one dominant LSZ, which led to the failure of whole sample.

The LSZ accumulated plastic strains continuously. Figure 2(c) shows heterogeneous εL at varying εapp as a result of the propagating LSZ. εL was measured along a longitudinal line which goes through the maximum εL (εmax) in each contour, e.g. white line at εapp = 1% in Figure 2(b). The LSZ is defined, here, as that with εL > εapp, e.g. the segment bounded by two × marks in the curve at εapp of 15.8%. Figure 2(d) shows the evolution of εmax and minimum εL (εmin) in NS layer. Note that εmax is always in the center of the LSZ. Figure 2(e) shows the evolution of average εL in LSZ, εLSZ. Figure 2(f) shows the axial maximum strain rate εL(εmax) in NS layer calculated by εL = dε/dt. εmax is found always at the propagating front of the LSZ and can be used as an indicator for the propagating rate of LSZ.

From Figure 2(b–f), several features of the plastic deformation can be drawn. Firstly, the shear band/LSZ sustained more strain in its interior than outside with increasing εapp (Figure 2(d)), typical of strain localization. The left and right peaks of εL, e.g. at εapp ≤ 6.8% (Figure 2(c)), represent the upper and the lower shear bands, while the latter disappeared at εapp = 15.8%. Secondly, εL is not uniform in the NS layer during the whole testing (Figure 2(b–d)). Moreover, εmax in shear band/LSZ is larger than εapp, even than EU (shadowed area in Figure 2(d)). In contrast, εL is equal to εapp in CG (see Figure S1 in the Supplementary Material), as represented by the diagonal dotted line, due to uniform deformation in the stable CG layer before necking. Thirdly, the ratio of εLSZ/εapp in the LSZ (Figure 2(e)) can be seen as an indicator on the severity of strain localization. As seen, strain localization started at low

**Figure 1.** Microstructure and Micro-hardness (HV) in GS IF steel. (a) Electron back-scatter diffraction image showing coarse-grains in the central CG layer. (b) TEM image showing nano-grains with high density of dislocations at ~40 μm depth in NS layer. (c) HV gradient along the depth.
Figure 2. Strain localization and delocalization in LSZ. (a) Tensile true stress–strain (σ–ε) curves measured by DIC testing. GS: gradient-structured sample. CG: coarse-grained sample. Square on each curve: uniform elongation (εU). (b) Contour maps of axial strain (εL) on NS surface vs. applied tensile strain (εapp). Surface area of the gauge section: 2 × 10 mm². Number above each map: εapp (%). Scale bar (color): range of εL in whole contour, with maximum (defined as εmax) (top number) and minimum εL (defined as εmin). Scale bar (horizontal): 2 mm. (c) Distribution of εL at varying εapp along axial position, e.g. white vertical line in the first contour in (d). (d) Maximum and minimum εL (εmax and εmin) vs. εapp. Diagonal dashed line: uniform εL of CG sample. (e) εLSZ/εapp vs. εapp, εLSZ: axial average strain in LSZ. Inset: Strain fraction supplied by the LSZ at varying εL. (f) Axial maximum strain rate (˙εL = dεL/dL) at the propagating front of the LSZ vs. εapp. (g) Profiles of lateral shrinkages in (b) at varying εapp (number, %). (h) Average lateral shrinkage rate at the upper LSZ vs. εapp.

εapp of ~1%, reached the maximum at εapp = 2.0%, and then decreased until the end of uniform elongation (E_U). Fourthly, ˙εmax started about one order of magnitude larger than ˙εapp = 8 × 10^-4 s^-1 (Figure 2(f)) and dropped monotonously. In other words, the shear band/LSZ propagated fast initially, but slowed down later. In contrast, the CG sample shows a nearly constant ˙εL until necking (Figure 2(f) and Figure S1 in SI). Most importantly, the applied strain is mostly sustained in the LSZ. The deformation fraction supplied by LSZ is calculated by (εLSZ × area of LSZ)/(εapp × gauge area). As seen in the inset of Figure 2(e), the LSZ accommodated the majority of the applied tensile strains.

Figure 2(g) shows the changing profiles of lateral shrinkage at varying εapp by subtracting local width from the largest real-time width. The location of localized shrinkage coincides with that of the LSZ, see the arrows in contour maps at varying εapp in Figure 2(b). In other words, the LSZ triggered localized lateral shrinkage at the very early stage. This is unexpected because the sample was still globally stable with strong strain hardening. Figure 2(h) shows the average lateral shrinkage rate ( ˙εT). It reached the peak at εapp ~ 5%, decreased subsequently, and increased again until global necking (E_U). In contrast, the CG sample has constant ˙εT, equal to half of ˙εapp, typical of uniform plastic deformation.
The heterogeneous $\varepsilon_L$ (Figure 2(c)) caused axial strain gradient, $d\varepsilon_L/dL$, near the LSZ boundaries in the NS layer. The maximum strain gradient lies always at the front of propagating LSZ, and increased with $\varepsilon_{\text{app}}$ (Figure 3(a)). Strain softening occurred in the center of the LSZ at the early stage of shear band formation (Figure 3(b)), showing dramatic drop of $H_V$. $H_V$ increased later with increasing $\varepsilon_{\text{app}}$ from 6.8% to 15.8%, indicating that it recovered some strain hardening capability (Figure 3(c)).

Strain gradient arises from mechanical incompatibility. The propagating front of the LSZ demarcates its boundary (Figure 3(b)). As shown, there is a steep strength gradient at the LSZ boundary, which will lead to strain gradient during tensile deformation. Geometrically necessary dislocations need to be produced to facilitate the strain gradient [27–29], which will produce strong back-stress hardening [14,30–36]. The back-stress hardening will impede the axial rapid propagation of the LSZ, which helps with the stabilization and delocalization of the shear band/the LSZ, leading to the drop of $\dot{\varepsilon}_L$ with $\varepsilon_{\text{app}}$ (Figure 2(g)).

The initial drop and later rise of $H_V$ in the center of the LSZ (Figure 3(b,c)) indicate the recovery of dislocation strain hardening. Figure 4(a) shows a weak compression shear texture with (110) orientation parallel to compressive axis due to SMAT before tensile testing (a-1), which evolved later into strong tensile textures with (110) orientation parallel to tensile axis at $\varepsilon_{\text{app}}$ of 15.8%. The tensile texture strength is especially strong at the center of the LSZ, as indicated in Figure 4(a-3), as compared with locations outside of the LSZ (as indicated in Figure 4(a-2). This indicates strong dislocation activities in nanograins in the LSZ during tensile deformation.

The dislocation activity is corroborated by TEM observations. At $\varepsilon_{\text{app}}$ of 4% (Figure 4(b)), the dislocations are hardly seen inside most grains in the center of the LSZ, in contrast to high density of dislocations before tensile testing (Figure 1(b)). Inset at the top left corner of Figure 4(b) reveals dislocation debris in a few grains. This indicates dismantlement of original dislocation sub-structure due to the change of strain path and stress state [12,37]. This is the reason of the observed strain softening in the shear band/LSZ (Figure 3(b)). Further straining led to the formation of new dislocation networks near grain boundaries, as shown in Figure 4(c) ($\varepsilon_{\text{app}} = 20.6\%$). This is caused by the complex stress state [12,37] in the LSZ, where multiple slip systems are activated, which in turn forms new dislocation entanglements and accumulation (see the inset). The change in dislocation density coincides with that of $H_V$ (Figure 3(c)), suggesting their close relationship. Furthermore, the mean grain size is maintained close to $\sim 200\text{ nm}$ in the LSZ during the tensile testing, indicating no grain growth in the LSZ.

It should be noted that initial softening and recovered hardening observed in the LSZ has some similarity and difference from the reported hardness fluctuation observed during the severe plastic deformation of a nanocrystalline Ni–Fe alloy [38]. Although both cases were linked to dislocation density change, the initial softening and recovered hardening in the LSZ was caused by the change of strain path, while the latter was observed during severe straining in the strain direction.

The NS layer and central CG layer in the GS sample were subjected to the same amount applied tensile strain. The NS layer deformed by propagating shear bands (Figure 2(b,c)), while the CG layer deformed uniformly. Strain delocalization in the shear bands/LSZ helped with retaining ductility in NS layer. In contrast, shear bands would have failed homogeneous NS metals quickly [2,3,11,12]. The LSZ regained strain hardening capability after the initial softening (Figure 4(c)), a phenomenon that would rarely occur in homogeneous NS metals [38]. Both forest dislocation hardening and

![Figure 3. Evolution of both maximum axial strain gradient ($\Psi_{\text{max}}$) and microhardness ($H_V$). (a) $\Psi_{\text{max}}$ at the front of the propagating LSZ vs. $\varepsilon_{\text{app}}$. (b) $H_V$ variation along axial LSZ at $\varepsilon_{\text{app}}$ of 6.8% and 15.8%. (c) Change of $H_V$ at the center of the LSZ vs. $\varepsilon_{\text{app}}$.](image)
Back-stress hardening occurred to stabilize the shear band [14,33], making it possible for its delocalization. The propagation of shear banding into the sample depth is deterred because the underneath CG layer is stable. This induces strain gradient in the depth direction and back-stress hardening to prevent the LSZ from propagating into the depth [12,31,34].

The strategy of utilizing the shear band delocalization to develop synergistic work hardening for improving the ductility is expected also applicable to other heterostructured metals consisting of NS and CG domains. Another way to delocalize strains caused by shear bands is to develop high-density of them all over the NS domains so that no individual shear band will fail the specimen. Similar synergistic work hardening as discussed above should also work in this situation to improve ductility. In fact, such types of LSZs have been observed in layered heterostructures although their effect on work hardening was not discussed [39].

In conclusion, strain localization by shear bands seems unavoidable in nanostructures. However, in GS materials the detrimental shear bands could be harnessed to benefit ductility. Specifically, in a gradient structured specimen shear bands nucleated early in the NS and propagated along the gage length, instead of across the specimen cross-section as normally observed in homogeneous materials. This delocalized the shear bands to form an LSZ. Strain gradient was produced in the propagating front of the LSZ, which produced back-stress hardening [14,34] to stabilize the propagating shear bands. In addition, strain gradient were also produced near the interfaces between the LSZ and CG central layer, which produces more back-stress hardening. Dislocation hardening capability in the LSZ was recovered after initial strain softening, which, along with back-stress hardening, induces synergistic strain hardening to help with ductility in NS layer.

**Impact statement**

We propose strategies for synergistic strain hardening in gradient structure by stabilizing shear band and strain gradients, turning harm of shear band into benefit of ductility.

**Disclosure statement**

No potential conflict of interest was reported by the authors.

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