Probing the R-parity violating supersymmetric effects in the exclusive $b \to c\ell^{-}\bar{\nu}_\ell$ decays

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Motivated by recent results from the LHCb, BABAR and Belle collaborations on $B \to D^{(*)}\ell^ {−}\bar{\nu}_\ell$ decays, which significantly deviate from the Standard Model and hint the possible new physics beyond the Standard Model, we probe the R-parity violating supersymmetric effects in $B_c^{-} \to \ell^{-}\bar{\nu}_\ell$ and $B \to D^{(*)}\ell^{-}\bar{\nu}_\ell$ decays. We find that (i) $\mathcal{B}(B_c^{-} \to e^{-}\bar{\nu}_e)$ and $\mathcal{B}(B_c^{-} \to \mu^{-}\bar{\nu}_\mu)$ are sensitive to the constrained slepton exchange couplings; (ii) the normalized forward-backward asymmetries of $B \to De^{-}\bar{\nu}_e$ decays have been greatly affected by the constrained slepton exchange couplings, and their signs could be changed; (iii) all relevant observables in the exclusive $b \to c\tau^ {−}\bar{\nu}_\tau$ decays and the ratios $\mathcal{R}(D^{(s)})$ are sensitive to the slepton exchange coupling, $\mathcal{R}(D^{*})$ could be enhanced by the constrained slepton exchange coupling to reach each 95% confidence level experimental range from BABAR, Belle and LHCb, but it could not reach the lower limit of the 95% confidence level experimental average. Our results in this work could be used to probe R-parity violating effects, and will correlate with searches for direct supersymmetric signals at the running LHCb and the forthcoming Belle-II.

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1 Introduction

The semileptonic decays $B \rightarrow D^{(*)}\ell^-\bar{\nu}_\ell$ are very important processes in testing the Standard Model (SM) and in searching for the new physics (NP) beyond the SM, for example, the extraction of the Cabbibo-Kobayashi-Maskawa matrix element $|V_{cb}|$. The semileptonic decays $B \rightarrow D^{(*)}\ell^-\bar{\nu}_\ell$ have been measured by the CLEO [1], Belle [2,3], BABAR [4–7] and LHCb [8] collaborations. For the ratios $R(D^{(*)}) \equiv \frac{B(B\rightarrow D^{(*)}\tau^-\bar{\nu}_\tau)}{B(B\rightarrow D^{(*)}\ell^-\bar{\nu}_\ell)}$ with $\ell' = e$ or $\mu$, the experimental averages from the Heavy Flavor Averaging Group [9] are

$$R(D)^{\text{Exp.}} = 0.391 \pm 0.050,$$
$$R(D^*)^{\text{Exp.}} = 0.322 \pm 0.021,$$

the SM predictions [10,11] are

$$R(D)^{\text{SM}} = 0.297 \pm 0.017,$$
$$R(D^*)^{\text{SM}} = 0.252 \pm 0.003,$$

the experimental measurements of $R(D)$ and $R(D^*)$ differ from their SM predictions by 1.7 $\sigma$ and 3.0 $\sigma$ deviations, respectively, and these hint the possible NP beyond the SM.

The exclusive $b \rightarrow c\ell^-\bar{\nu}_\ell$ decays have been studied extensively in the framework of the SM and various NP models, for instance, see Refs. [12–34]. The R-parity violating (RPV) supersymmetry (SUSY) is one of the respectable NP models that survived electroweak data [35–43]. In this paper, we will explore the RPV effects in the leptonic and semileptonic exclusive $b \rightarrow c\ell^-\bar{\nu}_\ell$ decays. We constrain relevant RPV parameter spaces from present experimental measurements and analyze their contributions to the branching ratios, the differential branching ratios, the normalized forward-backward (FB) asymmetries of the charged leptons, and the ratios of the branching ratios of relevant semileptonic $B$ decays.

The paper is organized as follows. In section 2, we briefly review the theoretical results of the exclusive $b \rightarrow c\ell^-\bar{\nu}_\ell$ decays in the RPV SUSY model. In section 3, using the constrained parameter spaces from relevant experimental measurements, we make a detailed classification research on the RPV effects on the quantities which have not been measured or not been well measured yet. Our conclusions are given in section 4.
2 The exclusive $b \to c \ell^- \bar{\nu}_\ell$ decays in the SUSY without R-parity

In the RPV SUSY model, the similar processes $b \to u \ell^- \bar{\nu}_\ell$ have been studied in Ref. 38, and we will only give the final expressions in this section.

The branching ratio for the pure leptonic decays $B^- \to \ell^- \bar{\nu}_\ell$ can be written as 38

$$\mathcal{B}(B^- \to \ell^- \bar{\nu}_\ell) = \left| \frac{G_F}{\sqrt{2}} V_{cb} - \sum_i \frac{\lambda'_{n3i} \tilde{\lambda}^*_{m2i}}{8 m^2_{d_{iR}}} \right|^2 + \sum_i \frac{\lambda_{innm} \tilde{\lambda}^*_{n2i} \mu_{B_n}}{4 m^2_{t_{iL}}} \left| \frac{2 \tau_{B_n} f^2_{B_n} m_{B_n} m_t^2}{4 \pi} \left( 1 - \frac{m_t^2}{m_{B_n}^2} \right)^2 \right|,$$

where $\mu_{B_n} \equiv m_{B_n}^2/(\bar{m}_b + \bar{m}_c)$.

The differential branching ratios for the semileptonic decays $B \to D \ell^- \bar{\nu}_\ell$ could be written as 38

$$\frac{d\mathcal{B}(B \to D \ell^- \bar{\nu}_\ell)}{dsdcos\theta} = \frac{\tau_B \sqrt{\lambda_D}}{2 \pi^3 m^3_B} \left( 1 - \frac{m^2_{\ell m}}{s} \right)^2 \left[ N^D_0 + N^D_1 \cos \theta + N^D_2 \cos^2 \theta \right],$$

with

$$N^D_0 = \left| \frac{G_F}{\sqrt{2}} V_{cb} - \sum_i \frac{\lambda'_{n3i} \tilde{\lambda}^*_{m2i}}{8 m^2_{d_{iR}}} \right|^2 \left| [f^D_+(s)]^2 \lambda_D + \frac{G_F}{\sqrt{2}} V_{cb} - \sum_i \frac{\lambda'_{n3i} \tilde{\lambda}^*_{m2i}}{8 m^2_{d_{iR}}} \right|^2 \frac{m^2_{\ell m} [f^D_+(s)]^2 (\bar{m}_b - \bar{m}_c)^2}{s},$$

$$N^D_1 = \left( \left| \frac{G_F}{\sqrt{2}} V_{cb} - \sum_i \frac{\lambda'_{n3i} \tilde{\lambda}^*_{m2i}}{8 m^2_{d_{iR}}} \right|^2 + \text{Re} \left( \left| \frac{G_F}{\sqrt{2}} V_{cb} - \sum_i \frac{\lambda'_{n3i} \tilde{\lambda}^*_{m2i}}{8 m^2_{d_{iR}}} \right|^2 \right) \right) \frac{2 m^2_{\ell m} f^D_+(s) f^D_+(s) \sqrt{\lambda_D (\bar{m}_b^2 - \bar{m}_c^2)}}{s},$$

$$N^D_2 = - \left| \frac{G_F}{\sqrt{2}} V_{cb} - \sum_i \frac{\lambda'_{n3i} \tilde{\lambda}^*_{m2i}}{8 m^2_{d_{iR}}} \right|^2 \left| [f^D_+(s)]^2 \lambda_D \left( 1 - \frac{m^2_{\ell m}}{s} \right) \right|,$$

The differential branching ratios for the semileptonic decays $B \to D^* \ell^- \bar{\nu}_\ell$ could be written as 38

$$\frac{d\mathcal{B}(B \to D^* \ell^- \bar{\nu}_\ell)}{dsdcos\theta} = \frac{\tau_B \sqrt{\lambda_{D^*}}}{2 \pi^3 m^3_B} \left( 1 - \frac{m^2_{\ell m}}{s} \right)^2 \left[ N^D_0 + N^D_1 \cos \theta + N^D_2 \cos^2 \theta \right],$$

with

$$N^{D^*}_0 = \left| \frac{G_F}{\sqrt{2}} V_{cb} - \sum_i \frac{\lambda'_{n3i} \tilde{\lambda}^*_{m2i}}{8 m^2_{d_{iR}}} \right|^2 \left( [A^D_1(s)]^2 \left( \frac{\lambda_{D^*}}{4 \bar{m}_{D^*}^2} + (m^2_{\ell m} + 2s) \right) (m_B + m_{D^*})^2 \right)$$
From above expressions, we can see that, unlike the contributions of the squark exchange $s$ be suppressed by $m_{\tilde{b}} - m_{\tilde{D}^*}$, the slepton exchange couplings $\lambda_{n3i} \tilde{\lambda}_{m2i}^{*}$ and the SM contributions, the slepton exchange couplings $\lambda_{imn} \tilde{\lambda}_{23}^{*}$ will not be suppressed by $s$ and helicity.

where $s = q^2 = (p_B - p_{D^{(*)}})^2$, the kinematic factor $\lambda_{D^{(*)}} = m_B^4 + m_D^{(*)4} + s^2 - 2m_B^2m_D^{(*)2} - 2m_B^2s - 2m_D^{(*)2}s$, and the $\theta$ is the angle between the momentum of $B$ meson and the charged lepton in the c.m. system of $\ell - \nu$.

The normalized forward-backward asymmetry of the charged lepton $\mathcal{A}_{FB}^{D^{(*)}}$ are given as

$$\mathcal{A}_{FB}(B \rightarrow D^{(*)} \ell^{-} \bar{\nu}_{\ell}) = \frac{N_{1}^{D^{(*)}}}{2N_{0}^{D^{(*)}}} + 2/3N_{2}^{D^{(*)}}.$$ (12)

From above expressions, we can see that, unlike the contributions of the squark exchange couplings $\lambda_{n3i} \tilde{\lambda}_{m2i}^{*}$ and the SM contributions, the slepton exchange couplings $\lambda_{imn} \tilde{\lambda}_{23}^{*}$ will not be suppressed by $s$ and helicity.
3 Numerical Results and Discussions

In the numerical calculations, the main theoretical input parameters are the transition form factors, the decay constant of $B_c^-$ meson, the masses, the mean lives, the CKM matrix element, etc. For the transition form factors, the traditional approaches to calculate the relevant transition form factors are the heavy quark effective theory [10, 23], the Lattice QCD techniques [12, 13] and the pQCD factorization approach with and without Lattice QCD input [26–28], we will use the form factors based on the heavy quark effective theory [10, 23]. The decay constant of $B_c^-$ meson is taken from Ref. [44], and the rest of the theoretical input parameters are taken from the Particle Data Group (PDG) [45]. Notice that we assume the masses of the corresponding sleptons are 500 GeV. For other values of the slepton masses, the bounds on the couplings in this paper can be easily obtained by scaling them by factor of $\tilde{f}^2 \equiv \left( \frac{m_{\tilde{\ell}}}{500 \text{GeV}} \right)^2$.

In our calculation, we consider only one NP coupling at one time and keep its interference with the SM amplitude to study the RPV SUSY effects. To be conservative, the input parameters and the experimental bounds except for $B(B \to D^*\tau^-\bar{\nu}_\tau)$ and $R(D^*)$ at 95% confidence level (CL) will be used to constrain parameter spaces of the relevant new couplings. Noted that we do not impose the experimental bounds from $B(B \to D^*\tau^-\bar{\nu}_\tau)$ and $R(D^*)$, since their experimental measurements obviously deviate from their SM predictions, and we leave them as predictions of the restricted parameter spaces of the RPV couplings, and then compare them with the experimental results.

Due to the strong helicity suppression, the squark exchange couplings have no very obvious effects on the differential branching ratios and the normalized FB asymmetries of the semileptonic exclusive $b \to c\ell^-\bar{\nu}_\ell$ decays. So we will only focus on the slepton exchange couplings in our follow discussions. For the slepton exchange couplings, $\lambda_{i11}\tilde{\lambda}'_{23}^{*}$ and $\lambda_{i22}\tilde{\lambda}'_{23}^{*}$, which contribute to both $b \to c\ell^-\bar{\nu}_\ell$ and $b \to s\ell^+\ell^-_{n}$ transitions, the stronger constraints are from the exclusive $b \to s\ell^+\ell^-_{n}$ decays [37, 41], nevertheless, the RPV weak phases of the two slepton exchange couplings are not obviously constrained by current experimental measurements.

3.1 The exclusive $b \to c\ell^-\bar{\nu}_\ell$ decays

First, we focus on slepton exchange couplings $\lambda_{i11}\tilde{\lambda}'_{23}^{*}$ contribute to five decay modes, $B_c^- \to e^-\bar{\nu}_e$, $B_u^- \to D_u^0e^-\bar{\nu}_e$, $B_d^- \to D_d^0e^-\bar{\nu}_e$, $B_s^0 \to D_s^+e^-\bar{\nu}_e$ and $B_d^0 \to D_d^{*+}e^-\bar{\nu}_e$ decays. The branching
Table 1: Branching ratios of the exclusive $b \to c e^- \bar{\nu}_e$ decays (in units of $10^{-2}$) except for $\mathcal{B}(B_c^- \to e^- \bar{\nu}_e)$ (in units of $10^{-9}$). The experimental ranges and the SM predictions at 95% CL are listed in the second and third columns, respectively. In the last column, “SUSY/$\lambda_{i11} \tilde{\lambda}^{e*}_{23}$” denotes the SUSY predictions considering the constrained $\lambda_{i11} \tilde{\lambda}^{e*}_{23}$ couplings. The similar in Table 2 and Table 3.

| Observable          | Exp. data | SM predictions | SUSY/$\lambda_{i11} \tilde{\lambda}^{e*}_{23}$ |
|---------------------|-----------|----------------|-----------------------------------------------|
| $\mathcal{B}(B_c^- \to e^- \bar{\nu}_e)$ | $\cdots$  | $[1.39, 2.72]$ | $[1.49 \times 10^{-2}, 1068]$ |
| $\mathcal{B}(B_u^- \to D_u^{0} e^- \bar{\nu}_e)$ | $[2.05, 2.49]$ | $[1.81, 2.91]$ | $[2.10, 2.49]$ |
| $\mathcal{B}(B_u^- \to D_u^{*0} e^- \bar{\nu}_e)$ | $[5.32, 6.06]$ | $[4.78, 5.81]$ | $[5.34, 5.61]$ |
| $\mathcal{B}(B_d^0 \to D_d^{*+} e^- \bar{\nu}_e)$ | $[1.95, 2.43]$ | $[1.68, 2.69]$ | $[1.96, 2.33]$ |
| $\mathcal{B}(B_d^0 \to D_4^{*+} e^- \bar{\nu}_e)$ | $[4.71, 5.15]$ | $[4.44, 5.38]$ | $[4.89, 5.15]$ |

ratios of four semileptonic processes have been accurately measured by CLEO [1], Belle [2] and BABAR [5,6] collaborations. The 95% CL ranges of the experimental average values from the PDG [45] are listed in the second column of Table 1. The SM predictions at 95% CL are presented in the third column of Table 1.

Using the experimental bounds of relevant exclusive $b \to c \ell^- \bar{\nu}_\ell$ decays at 95% CL, we obtain the slepton exchange couplings $|\lambda_{i11} \tilde{\lambda}^{\ell*}_{23}| \leq 0.22$. At present, the strongest bounds on the slepton exchange couplings come from the exclusive $b \to s e^+ e^-$ decays, $|\lambda_{i11} \tilde{\lambda}^{e*}_{23}| \leq 5.75 \times 10^{-4}$ with 500 GeV slepton masses [37], which will be used in our numerical results. In addition, the experimental bounds at the 95% CL listed in the second column of Table 1 are also considered to further constrain the slepton exchange couplings. Our numerical results of relevant branching ratios, which consider the constrained slepton exchange couplings, are listed in the last column of Table 1 and we can see that the constrained slepton exchange coupling has significant effects on $\mathcal{B}(B_c^- \to e^- \bar{\nu}_e)$, which could be suppressed 2 orders or enhanced 3 orders by the constrained slepton exchange couplings. Nevertheless, the constrained slepton exchange couplings have no significant effects on the branching ratios of relevant semileptonic decays.

For $B_u^- \to D_u^{(*)0} e^- \bar{\nu}_e$ and $B_d^0 \to D_d^{(*)+} e^- \bar{\nu}_e$ decays, since the $SU(3)$ flavor symmetry implies $\mathcal{M}(B_u^- \to D_u^{(*)0} e^- \bar{\nu}_e) \simeq \mathcal{M}(B_d^0 \to D_d^{(*)+} e^- \bar{\nu}_e)$, the slepton exchange RPV contributions to $B_u^- \to D_u^{(*)0} e^- \bar{\nu}_e$ and $B_d^0 \to D_d^{(*)+} e^- \bar{\nu}_e$ are very similar to each other. So we would take
Figure 1: The constrained slepton exchange coupling effects in the exclusive $b \to c e^- \bar{\nu}_e$ decays.

$B^- \to D^{(*)0}e^- \bar{\nu}_e$ decays as examples. The similar in the exclusive $b \to c \mu^- \bar{\nu}_\mu$ and $b \to c \tau^- \bar{\nu}_\tau$ decays.

Fig. (a-b) shows the constrained RPV effects of $\lambda_{i11}\tilde{\lambda}^*_{i23}$ on $B(B^- \to e^- \bar{\nu}_e)$, $d\mathcal{B}(B_u^- \to D^{(*)0}e^- \bar{\nu}_e)/ds$, and $\mathcal{A}_{FB}(B_u^- \to D^{(*)0}e^- \bar{\nu}_e)$. The SM results are also displayed for comparing. Comparing the RPV SUSY predictions to the SM ones, we have the following remarks.

- As shown in Fig. (a-b), $B(B_c^- \to e^- \bar{\nu}_e)$ is very sensitive to both moduli and weak phases
of the $\lambda_{i11}\tilde{\lambda}_{23}^{*}$ couplings, and this is due to that the slepton exchange coupling effects on $B(B_{c}^{-}\to e^{-}\bar{\nu}_{e})$ is increased by $m_{B}/m_{e}$.

- As displayed in Fig. 1 (c-d), there are no obvious RPV effect on $dB(B_{u}^{-}\to D_{u}^{0}e^{-}\bar{\nu}_{e})$, since the present accurate experimental measurements of $B(B_{u}^{-}\to D_{u}^{0}e^{-}\bar{\nu}_{e}, B_{d}^{0}\to D_{d}^{+}e^{-}\bar{\nu}_{e})$ give very strongly constraints on the slepton exchange couplings. For the same reason, the branching ratios of relevant semileptonic decays are not sensitive to both moduli and weak phases of the $\lambda_{i11}\tilde{\lambda}_{23}^{*}$ couplings, so we do not display them in Fig. 1.

- Fig. 1 (e) shows us that the constrained $\lambda_{i11}\tilde{\lambda}_{23}^{*}$ couplings provide quite obvious effects on $\tilde{A}_{FB}(B_{u}^{-}\to D_{u}^{0}e^{-}\bar{\nu}_{e})$, its sign could be changed, nevertheless, this quantity is tiny.

Fig. 1 (f) shows that there is no obvious RPV effect on $\tilde{A}_{FB}(B_{u}^{-}\to D_{u}^{0}e^{-}\bar{\nu}_{e})$.

### 3.2 The exclusive $b\to c\mu^{-}\bar{\nu}_{\mu}$ decays

Now we pay attention to the contributions of the slepton exchange couplings $\lambda_{i22}\tilde{\lambda}_{23}^{*}$ to $B_{c}^{-}\to \mu^{-}\bar{\nu}_{\mu}, B_{d}^{0}\to D_{d}^{0}\mu^{-}\bar{\nu}_{\mu}, B_{u}^{-}\to D_{u}^{0}\mu^{-}\bar{\nu}_{\mu}, B_{d}^{0}\to D_{d}^{+}\mu^{-}\bar{\nu}_{\mu}$ decays. The four semi-leptonic decay branching ratios have been accurately measured by CLEO [1], Belle [2] and BABAR [5,6] collaborations. The experimental average values and the SM predictions at 95% CL are listed in the second and third column of Table 2 respectively.

We get the slepton exchange couplings $|\lambda_{i22}\tilde{\lambda}_{23}^{*}| < 0.24$ from the exclusive $b\to c\ell^{-}\bar{\nu}_{\ell}$ decays, which are a lot weaker than ones from the exclusive $b\to s\mu^{+}\mu^{-}$ decays, $|\lambda_{i22}\tilde{\lambda}_{23}^{*}| < 2.0 \times 10^{-4}$.

Table 2: Branching ratios of the exclusive $b\to c\mu^{-}\bar{\nu}_{\mu}$ decays (in units of $10^{-2}$) except for $B(B_{c}^{-}\to \mu^{-}\bar{\nu}_{\mu})$ (in units of $10^{-4}$).

| Observable | Exp. data | SM predictions | SUSY/$\lambda_{i22}\tilde{\lambda}_{23}^{*}$ |
|------------|-----------|----------------|------------------------------------------|
| $B(B_{c}^{-}\to \mu^{-}\bar{\nu}_{\mu})$ | $\cdots$ | $[0.59, 1.16]$ | $[0.51, 1.17]$ |
| $B(B_{u}^{-}\to D_{u}^{0}\mu^{-}\bar{\nu}_{\mu})$ | $[2.05, 2.49]$ | $[1.81, 2.89]$ | $[2.09, 2.48]$ |
| $B(B_{u}^{-}\to D_{u}^{0}\mu^{-}\bar{\nu}_{\mu})$ | $[5.32, 6.06]$ | $[4.76, 5.77]$ | $[5.32, 5.59]$ |
| $B(B_{d}^{-}\to D_{d}^{+}\mu^{-}\bar{\nu}_{\mu})$ | $[1.95, 2.43]$ | $[1.68, 2.67]$ | $[1.96, 2.32]$ |
| $B(B_{d}^{0}\to D_{d}^{+}\mu^{-}\bar{\nu}_{\mu})$ | $[4.71, 5.15]$ | $[4.42, 5.35]$ | $[4.87, 5.13]$ |
Figure 2: The constrained slepton exchange coupling effects in the exclusive $b \rightarrow c \mu^- \bar{\nu}_\mu$ decays.

With 500 GeV slepton masses [41]. Taking the strongest bounds from the exclusive $b \rightarrow s \mu^+ \mu^-$ decays and further considering the experimental bounds from the exclusive $b \rightarrow c \ell^- \bar{\nu}_\ell$ decays, we predict the constrained slepton exchange effects in the exclusive $b \rightarrow c \mu^- \bar{\nu}_\mu$ decays, which are given in the last column of Table 2 and displayed in Fig. 2. From Table 2 and Fig. 2, we make the following points.

- As displayed in Fig. 2 (a-b), $B(B_c^- \rightarrow \mu^- \bar{\nu}_\mu)$ has some sensitivities to both modulus and
3.3 The exclusive $b \rightarrow c\tau^-\bar{\nu}_\tau$ decays

In this subsection, we concentrate on the contributions of the slepton exchange couplings $\lambda_{i33}\tilde{\lambda}_{i23}^{\ast}$ in $B_c^- \rightarrow \tau^-\bar{\nu}_\tau$, $B_u^- \rightarrow D_u^0\tau^-\bar{\nu}_\tau$, $B_u^- \rightarrow D_u^0\tau^-\bar{\nu}_r$, $B_d^0 \rightarrow D_d^+\tau^-\bar{\nu}_r$ and $B_d^0 \rightarrow D_d^+\tau^-\bar{\nu}_\tau$ decays. The precise measurements of these semileptonic branching ratios have been reported by BABAR, Belle and LHCb [3,4,7,8]. The 95% CL experimental ranges of the average data from PDG [45] and the 95% CL SM predictions are listed in the second and the third columns of Table 3, respectively.

Fig. 3 displays the allowed parameter spaces of the couplings $\lambda_{i33}\tilde{\lambda}_{i23}^{\ast}$ from the 95% CL experimental bounds of the exclusive $b \rightarrow c\ell^-\bar{\nu}_\ell$ decays. Both the moduli and the weak phases of the $\lambda_{i22}\tilde{\lambda}_{i23}^{\ast}$ couplings, and it has maximum at $\phi_{RPV} \in [-60^\circ, 60^\circ]$.

- Fig. 2 (c-d) shows that the constrained slepton exchange couplings have no obvious contribution to $dB(B_u^- \rightarrow D_u^{(s)0}\mu^-\bar{\nu}_\mu)/ds$, and they are strongly constrained by present experimental data.

- As displayed in Fig. 2 (e-f), the constrained slepton exchange couplings also have no obvious contribution to $\bar{A}_{FB}(B_u^- \rightarrow D_u^{(s)0}\mu^-\bar{\nu}_\mu)$ at all $s$ range. Noted that, the slepton exchange coupling effects on $\bar{A}_{FB}(B_u^- \rightarrow D_u^0\mu^-\bar{\nu}_\mu)$ are very different from ones on $\bar{A}_{FB}(B_u^- \rightarrow D_u^0\tau^-\bar{\nu}_\tau)$ displayed in Fig. 1 (e-f), since the bounds on $|\lambda_{i22}\tilde{\lambda}_{i23}^{\ast}|$ are about 3 times smaller than ones on $|\lambda_{i11}\tilde{\lambda}_{i23}^{\ast}|$ (the same order of magnitude) and $\bar{A}_{FB}(B_u^- \rightarrow D_u^0\mu^-\bar{\nu}_\mu)$ is 1000 times larger than $\bar{A}_{FB}(B_u^- \rightarrow D_u^0\tau^-\bar{\nu}_\tau)$.

| Observable | Exp. data | SM predictions | SUSY/$\lambda_{i33}\tilde{\lambda}_{i23}^{\ast}$ |
|------------|-----------|----------------|---------------------------------------------|
| $\mathcal{B}(B_c^- \rightarrow \tau^-\bar{\nu}_\tau)$ | ⋯ | [1.42, 2.78] | [0.87, 100] |
| $\mathcal{B}(B_u^- \rightarrow D_u^0\tau^-\bar{\nu}_\tau)$ | [0.28, 1.26] | [0.52, 0.90] | [0.64, 1.20] |
| $\mathcal{B}(B_u^- \rightarrow D_u^0\tau^-\bar{\nu}_r)$ | [1.49, 2.27] | [1.21, 1.47] | [1.21, 1.53] |
| $\mathcal{B}(B_u^- \rightarrow D_u^0\tau^-\bar{\nu}_\tau)$ | [0.60, 1.46] | [0.48, 0.84] | [0.60, 1.12] |
| $\mathcal{B}(B_d^0 \rightarrow D_d^+\tau^-\bar{\nu}_r)$ | [1.41, 2.27] | [1.12, 1.36] | [1.12, 1.41] |
Figure 3: The allowed parameter spaces of $\lambda_{i33} \tilde{\lambda}^*_{i23}$ from the 95% CL experimental bounds of the exclusive $b \to c\ell^-\bar{\nu}_\ell$ decays.

of $\lambda_{i33} \tilde{\lambda}^*_{i23}$ are obviously constrained by current experimental measurement. The bounds on $\lambda_{i33} \tilde{\lambda}^*_{i23}$ is obtained for the first time.

Now we discuss the constrained $\lambda_{i33} \tilde{\lambda}^*_{i23}$ effects in the exclusive $b \to c\tau^-\bar{\nu}_\tau$ decays. Our numerical predictions are given in the last column of Table 3. Fig. 4 shows the sensitivities of branching ratios to both moduli and weak phases of $\lambda_{i33} \tilde{\lambda}^*_{i23}$, and Fig. 5 shows the constrained slepton exchange effects on the differential branching ratios and the normalized FB asymmetries of $B^- \to D_u^{(*)0}\tau^-\bar{\nu}_\tau$ decays.

As displayed in Fig. 4 (a-b), $B(B_c^- \to \tau^-\bar{\nu}_\tau)$ is very sensitive to both moduli and weak phases of $\lambda_{i33} \tilde{\lambda}^*_{i23}$, so the future experimental measurements on $B(B_c^- \to \tau^-\bar{\nu}_\tau)$ will give quite strong bound on $\lambda_{i33} \tilde{\lambda}^*_{i23}$. As displayed in Fig. 4 (c-d), $B(B_u^- \to D_u^{0}\tau^-\bar{\nu}_\tau)$ is sensitive to $|\lambda_{i33} \tilde{\lambda}^*_{i23}|$ but not very sensitive to their weak phases. We also can see that present experimental measurements of $R(D)$ give strong bounds on this branching ratio. As displayed in Fig. 4 (e-f), $B(B_u^- \to D_u^{(*)0}\tau^-\bar{\nu}_\tau)$ is very sensitive to both moduli and weak phases of $\lambda_{i33} \tilde{\lambda}^*_{i23}$ couplings, $B(B_u^- \to D_u^{(*)0}\tau^-\bar{\nu}_\tau)$ could have maximum at $|\lambda_{i33} \tilde{\lambda}^*_{i23}| \in [0.1, 0.2]$ and $\phi_{RPV} \in [-60^\circ, 60^\circ]$, and they could catch the lower limits of present 95% CL experimental averages.
Figure 4: The constrained effects of the slepton exchange coupling $\lambda_{i33}\bar{\lambda}_{i23}^*$ in the exclusive $b \rightarrow c\tau^-\bar{\nu}_\tau$ decays.

In Fig. 5(a), we show another RPV prediction with the green “-” labeled with “SM+RPVII”, which is constrained by all above mentioned 95% CL experimental measurements except $R(D)$. We can see that the constrained $\lambda_{i33}\bar{\lambda}_{i23}^*$ couplings have very large effects on $dB(B_u \rightarrow D^0_\tau\tau^-\bar{\nu}_\tau)/ds$ at whole $s$ regions, and the 95% CL experimental bound of $R(D)$ give quite obvious constraints at middle and high $s$ regions. Fig. 5 (b) shows us that the constrained $\lambda_{i33}\bar{\lambda}_{i23}^*$ couplings have
some effects on $dB(B^{-}_u \rightarrow D^{(*)0}_u \tau^{-}\bar{\nu}_\tau)/ds$ at the middle $s$ region. As displayed in Fig. 5 (c-d), the constrained $\lambda_{i33}\lambda'_{i23}$ couplings have significant effects on $\bar{A}_{FB}(B^{-}_u \rightarrow D^{(*)0}_u \tau^{-}\bar{\nu}_\tau)$ at whole $s$ region.

### 3.4 The ratios $\mathcal{R}(D)$ and $\mathcal{R}(D^*)$

For the exclusive $b \rightarrow c\ell^{-}\bar{\nu}_\ell$ decays, the ratios of the branching ratios have been accurately measured by LHCb, BABAR and Belle [3, 4, 7, 8]. At 95% CL, their experimental averaged ranges, the SM predictions and the RPV SUSY predictions are listed in Table 4. We can see that $\mathcal{R}(D)$ is constrained by its 95% CL experimental measurements. As for $\mathcal{R}(D^*)$, the maximum of the RPV prediction is almost reach the lower limit of its 95% CL experimental measurements.

In order to compare easily, we display the 95% CL SM predictions, the 95% CL RPV SUSY
Table 4: The ratios $R(D)$ and $R(D^*)$ in the exclusive $b \to c\ell^-\bar{\nu}_\ell$ decays.

|       | $R(D)$       | $R(D^*)$     |
|-------|--------------|--------------|
|       | [0.294, 0.488] | [0.280, 0.364] |
|       | [0.251, 0.343] | [0.242, 0.263] |
|       | [0.294, 0.488] | [0.226, 0.278] |

Figure 6: The ratios $R(D)$ and $R(D^*)$. The theoretical predictions and experimental measurements from BABAR, Belle and LHCb are shown at 95% CL, and the experiential average are given within 5σ. The error of the experiential average is much smaller than each one of measurements from BABAR, Belle as well as LHCb, and their experimental average within 5σ on the $R(D)$-$R(D^*)$ plane in Fig. [6] and we can clearly see that our RPV SUSY predictions have about 2σ deviations from the experimental averaged values on the $R(D)$-$R(D^*)$ plane. At 95% CL, the RPV SUSY predictions of $R(D)$ and $R(D^*)$ are consistent with each experimental measurement from BABAR, Belle and LHCb. The error of the experiential average is much smaller than each one of measurements from BABAR, Belle and LHCb, at 99% CL, the RPV SUSY predictions for $R(D)$ and $R(D^*)$ agree with the experimental averages.

Now we give the sensitivities of $R(D^{(*)})$ to the slepton exchange couplings. Since the
Figure 7: The constrained effects of RPV coupling $\lambda_{i33}\tilde{\lambda}_{i23}^*$ due to the slepton exchange in the ratios $R(D^{(*)})$.

The ratios $R(D)$ and $R(D^*)$ are not sensitive to $\lambda_{i11}\tilde{\lambda}_{i23}^*$ and $\lambda_{i22}\tilde{\lambda}_{i23}^*$ couplings, we only show the sensitivities to the moduli and weak phases of $\lambda_{i33}\tilde{\lambda}_{i23}^*$ couplings in Fig. 7. As displayed in Fig. 7 (a-b), $R(D)$ is sensitive to $|\lambda_{i33}\tilde{\lambda}_{i23}^*|$ coupling, and the experimental average of $R(D)$ gives obvious constraints on $|\lambda_{i33}\tilde{\lambda}_{i23}^*|$. In Fig. 7 (c-d), $R(D^*)$ is very sensitive to both moduli and weak phases of the $\lambda_{i33}\tilde{\lambda}_{i23}^*$ couplings, it could have maximum at $|\lambda_{i33}\tilde{\lambda}_{i23}^*| \in [0.1, 0.2]$ and $\phi_{RPV} \in [-60^\circ, 60^\circ]$.

4 Conclusion

Motivated by the recent experimental data of the ratios $R(D^{(*)})$ reported by LHCb, BABAR and Belle collaborations, we have studied the RPV SUSY effects in the leptonic and semileptonic decays, $B_c^- \rightarrow \ell^- \bar{\nu}_\ell$, $B_u^- \rightarrow D_u^0 \ell^- \bar{\nu}_\ell$, $B_u^- \rightarrow D_u^{*0} \ell^- \bar{\nu}_\ell$, $B_d^0 \rightarrow D_d^+ \ell^- \bar{\nu}_\ell$, $B_d^0 \rightarrow D_d^{*+} \ell^- \bar{\nu}_\ell$. 

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Considering the theoretical uncertainties and the experimental errors at 95% CL, we have con-
strained the parameter spaces of relevant RPV couplings from the present experimental data.
We have found that the effects of the squark exchange couplings could be neglect in the exclu-
sive \( b \rightarrow c\ell^-\bar{\nu}_\ell \) decays. As for the slepton exchange couplings, the strongest bounds on \( \lambda_{i11}\tilde{\lambda}_{123}^s \) and \( \lambda_{i22}\tilde{\lambda}_{123}^s \) came from the exclusive \( b \rightarrow s\ell^+\ell^- \) decays, and the bounds on \( \lambda_{i33}\tilde{\lambda}_{123}^s \) have been obtained from the exclusive \( b \rightarrow c\ell^-\bar{\nu}_\ell \) decays for the first time.

Furthermore, we have predicted the constrained slepton exchange effects on the branching
ratios, the differential branching ratios and the normalized FB asymmetries of the charged
leptons, the ratios of the semilepton decay branching ratios. We have found that \( B(B_c^+ \rightarrow \ell^-\bar{\nu}_\ell) \)
and \( B(B \rightarrow D^*\tau^-\bar{\nu}_\tau) \) are very sensitive to the constrained slepton exchange couplings, and the
constrained slepton exchange couplings have great effects on \( d\mathcal{B}(B \rightarrow D\tau^-\bar{\nu}_\tau)/ds \), \( \mathcal{A}_{FB}(B \rightarrow De^-\bar{\nu}_e) \), \( \mathcal{A}_{FB}(B \rightarrow D\tau^-\bar{\nu}_\tau) \) and \( \mathcal{A}_{FB}(B \rightarrow D^*\tau^-\bar{\nu}_\tau) \), in addition, the sign of \( \mathcal{A}_{FB}(B \rightarrow De^-\bar{\nu}_e) \)
could be changed by the large slepton exchange couplings \( \lambda_{i11}\tilde{\lambda}_{123}^s \).

For \( \mathcal{R}(D) \) and \( \mathcal{R}(D^*) \), they are very sensitive to the constrained \( \lambda_{i33}\tilde{\lambda}_{123}^s \) couplings, but
not sensitive to the constrained \( \lambda_{i11}\tilde{\lambda}_{123}^s \) and \( \lambda_{i22}\tilde{\lambda}_{123}^s \) couplings from the exclusive \( b \rightarrow s\ell^+\ell^- \)
decays. The constrained \( \lambda_{i33}\tilde{\lambda}_{123}^s \) couplings could enhance \( \mathcal{R}(D) \) to its 95% CL experimental
range. Although the constrained \( \lambda_{i33}\tilde{\lambda}_{123}^s \) couplings maybe enhance \( \mathcal{R}(D^*) \), its maximum still
has 2\( \sigma \) deviation from the 95% CL experimental average. Nevertheless, the constrained slepton
exchange couplings could let \( \mathcal{R}(D^*) \) to reach each 95% CL experimental range from BABAR,
Belle and LHCb. In addition, at 99% CL, the RPV prediction for \( \mathcal{R}(D^*) \) agrees with the
experimental averages.

With the running LHCb and the forthcoming Belle-II experiments, heavy flavor physics
is entering a precision era, which would present new features to examine various NP models,
including the RPV SUSY model studied in this paper. Our results could be useful for probing
the RPV SUSY effects, and will correlate strongly with searches for the direct RPV SUSY
signals at future experiments.

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