SECTION 7. Mechanics and machine construction.

DEFORMATIONS ISOSURFACES OF CANTILEVER AND DOUBLY SUPPORTED STEEL I-BEAMS AT BENDING

Abstract: The calculation of deformed state of cantilever and doubly supported steel I-beams after removing of concentrated or distributed loads is presented in the article. Isosurfaces of deformation tensor of the I-beams material for all components are calculated. The conclusion about direction and intensity of volumetric deformation of the I-beams material by the color isosurfaces is given.

Key words: an I-beam, deformation, concentrated and distributed forces, moment, tensor, a component.

Language: Russian English

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Introduction
Description of stress-strain state of metal I-beams is presented in the works [1 – 10].
Applied external loads lead to bending of the I-beams and versatile volumetric deformation in material. Rotation of the I-beam at a certain angle occurs during bending. This process leads to displacement of material layers of the I-beam throughout a volume. Deformations of tensile or compressive that reduce strength of material occur in the inner layers of the I-beam.

Problems solving in the discipline "Technical mechanics" allows to get an overall assessment of stress state of the I-beams. Volumetric plastic deformation of the I-beam material is determined by deformation tensor. A three-dimensional view of deformation of the beam material can be obtained in a short period of time by finite element modeling.

Recommendations for a choice of cross sectional dimensions of the cantilever and doubly supported I-beams can be formulated in accordance with the conclusion about a degree of plastic deformation of material.

Materials and methods
Solid models of the I-beams were subjected to loads that have been applied in the COMSOL Multiphysics software environment. Deformation of the cantilever and doubly supported I-beams was calculated. Concentrated and distributed forces, concentrated moment were applied. The loading schemes of the models of the cantilever and doubly supported I-beams are presented in the table 1.

The calculation of the cantilever and doubly supported I-beams was carried out taking into account the reliability factor in relation to loading by the value of 1.2 and the own weight of the beam.

Structural steel has been adopted as material of the I-beam models. Young's modulus and calculated resistance of the beams material were adopted by the values of 206000 and 230 MPa, respectively.

The main characteristics of the I-beams:
- the weight of one running meter of the beam \( q \approx 8.1 \text{ kg/m} \);
- inertia moment \( J_x \approx 171 \text{ cm}^4 \);
- moment of resistance \( W_x \approx 34.2 \text{ cm}^3 \);
- static moment of a half-section \( S_x \approx 19.7 \text{ cm}^3 \);
- a web thickness \( t \approx 4.1 \text{ mm} \).

Results and discussion
The isosurfaces of rotation of deformation tensor on the solid models of the loaded I-beams are presented in the Fig. 1 – 9.

The \( xX \), \( yY \) and \( zZ \) components of deformation tensor of material of the cantilever and doubly supported I-beams are zero, i.e. deformation is not observed. The isosurfaces of material deformation of the I-beams mostly have the negative values. This suggests that the beam material is dominated by compressive deformation.

The values of the deformation coefficients were determined for two components \((yZ \text{ and } zY)\) of deformation tensor of the cantilever I-beams. The deformation coefficients of material have the negative values under the action of concentrated moment clockwise and concentrated force on a loose end of the I-beam. The deformation coefficients of material have the positive values under the action of concentrated force at \(1/2\) of a span length and distributed force at the entire span length of the I-beam. The positive and negative values of the deformation coefficients of material are observed in other components.

Maximum deformation of compressive and tensile of material of the cantilever I-beam (the loading scheme No. 2) was noted in the planes \( zY \left( -7.53 \times 10^{-4} \right) \) and \( yZ \left( 7.53 \times 10^{-4} \right) \), respectively.

Bending leads to deflection of the cantilever and doubly supported I-beams. The deflection value of the I-beams characterizes strength and rigidity of material of a construction element. The values of maximum deflections of the cantilever and doubly supported I-beams are presented in the summary table 2.

Maximum deflection of the beam was determined for the second loading scheme (the cantilever I-beam), minimum deflection was determined for the ninth loading scheme (the doubly supported I-beam).

Conclusion
The layers of material which are oriented along the length and the height of the cantilever I-beam are subjected to maximum deformation.

Loading of the I-beam according to the second scheme leads to maximum deflection which is \( 1/175 \) from the maximum span of the beam.

The additional support (at the considered span length) gives rigidity increasing of the I-beam by about 6 times.

Table 1. The loading schemes of the cantilever and doubly supported I-beams.

![Image](image-url)
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A – the first scheme; B – the second scheme; C – the third scheme; D – the fourth scheme; E – the fifth scheme; F – the sixth scheme; G – the seventh scheme; H – the eighth scheme; I – the ninth scheme.
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Figure 1 – Rotation of deformation tensor, xX component: A – the first scheme; B – the second scheme; C – the third scheme; D – the fourth scheme; E – the fifth scheme; F – the sixth scheme; G – the seventh scheme; H – the eighth scheme; I – the ninth scheme.
Figure 2 – Rotation of deformation tensor, $xY$ component: $A$ – the first scheme; $B$ – the second scheme; $C$ – the third scheme; $D$ – the fourth scheme; $E$ – the fifth scheme; $F$ – the sixth scheme; $G$ – the seventh scheme; $H$ – the eighth scheme; $I$ – the ninth scheme.
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Figure 3 – Rotation of deformation tensor, xZ component: A – the first scheme; B – the second scheme; C – the third scheme; D – the fourth scheme; E – the fifth scheme; F – the sixth scheme; G – the seventh scheme; H – the eighth scheme; I – the ninth scheme.
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**Figure 4** – Rotation of deformation tensor, yX component: 
- **A** – the first scheme; 
- **B** – the second scheme; 
- **C** – the third scheme; 
- **D** – the fourth scheme; 
- **E** – the fifth scheme; 
- **F** – the sixth scheme; 
- **G** – the seventh scheme; 
- **H** – the eighth scheme; 
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| BI (India)       | 4.260         |
| ICV (Poland)     | 6.630         |

Figure 5 – Rotation of deformation tensor, yY component: A – the first scheme; B – the second scheme; C – the third scheme; D – the fourth scheme; E – the fifth scheme; F – the sixth scheme; G – the seventh scheme; H – the eighth scheme; I – the ninth scheme.
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| JIF                      | 1.500         |
| SJIF (Morocco)           | 5.667         |
| OAJI (USA)               | 0.350         |

**Figure 6** – Rotation of deformation tensor, yZ component: A – the first scheme; B – the second scheme; C – the third scheme; D – the fourth scheme; E – the fifth scheme; F – the sixth scheme; G – the seventh scheme; H – the eighth scheme; I – the ninth scheme.
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Figure 7 – Rotation of deformation tensor, zX component: A – the first scheme; B – the second scheme; C – the third scheme; D – the fourth scheme; E – the fifth scheme; F – the sixth scheme; G – the seventh scheme; H – the eighth scheme; I – the ninth scheme.
Figure 8 – Rotation of deformation tensor, zY component: A – the first scheme; B – the second scheme; C – the third scheme; D – the fourth scheme; E – the fifth scheme; F – the sixth scheme; G – the seventh scheme; H – the eighth scheme; I – the ninth scheme.
Figure 9 – Rotation of deformation tensor, $zZ$ component: $A$ – the first scheme; $B$ – the second scheme; $C$ – the third scheme; $D$ – the fourth scheme; $E$ – the fifth scheme; $F$ – the sixth scheme; $G$ – the seventh scheme; $H$ – the eighth scheme; $I$ – the ninth scheme.
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| OAJI (USA)    | 0.350         |
| RINC (Russia) | 0.156         |
| ESJI (KZ)     | 8.716         |

Table 2. Maximum deflections of the I-beams.

| The scheme number | 1st   | 2nd   | 3rd   | 4th   | 5th   | 6th   | 7th   | 8th   | 9th   |
|-------------------|-------|-------|-------|-------|-------|-------|-------|-------|-------|
| Maximum deflection, mm | 1.74  | 5.71  | 1.81  | 2.16  | 0.22  | 0.36  | 0.23  | 0.31  | 0.12  |

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