Changes of Event Size Distribution During Episodes of Shallow Tectonic Tremor, Nankai Trough

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Abstract Slow earthquakes follow a power-law size distribution with an exponential taper for the largest events. We investigated changes in the size distribution of shallow tectonic tremor events during two prolonged tremor episodes (>1 month) along the Nankai trough and found that the slope of the size distributions increased while the cut-off magnitudes decreased late during each episode, as tremor activity waned. Interpreting these changes with the two-dimensional probabilistic cell automaton model of slow earthquakes, we found that a decrease in event ignition probability or an increase in energy dissipation during slip can qualitatively explain the observed changes. These changes imply that a decrease in accumulated stress or pore-fluid pressure on the fault interface occurred during each tremor episode. Because the tremor source migrates during an episode, the changes in the size distribution parameters can be attributed to spatial variations or temporal changes in the source characteristics.

Plain Language Summary The size distribution of slow earthquakes mostly follows a power law like that of ordinary earthquakes, in which the logarithm of event numbers is negatively proportional to the logarithm of event sizes, with an exponential taper for events larger than a cut-off magnitude. We investigated the changes in this size distribution during two prolonged episodes of shallow tectonic tremor that occurred on the plate interface along the Nankai trough, southwestern Japan. We found that the ratio of smaller events increased and the cut-off magnitude decreased as tremor activity decreased late in each episode. We interpreted this observation by using a model of slow earthquakes that divides a source fault into small cells and updates slip on each cell probabilistically. The model can explain the changes in the tremor size distribution by a decrease in the probability of event ignition or an increase in the energy dissipation during fault slip. This result implies that the accumulated stress or the pore-fluid pressure on the source fault decreased when the tremor was less active. Because the tremor source migrates during the course of each episode, these changes indicate that the source characteristics of tremor vary at different times or locations.

1. Introduction

Slow earthquakes, fault slips with longer durations than ordinary earthquakes of similar magnitudes, mostly occur in areas surrounding the source regions of megathrust earthquakes in subduction zones (e.g., Obara & Kato, 2016). Signals of a slow earthquake may be termed as tectonic tremor, a very low frequency earthquake (VLFE), or a slow slip event (SSE) depending on the frequency band of the observations, all of which share common fault slips because they occur concurrently in the same source region (e.g., Araki et al., 2017; Ito et al., 2007; Kaneko et al., 2018; Obara & Hirose, 2006; Obara et al., 2004; Rogers & Dragert, 2003). The source process of slow earthquakes is studied through the analysis of scaling relationships among the source characteristics: event duration, recurrence interval, size of the source fault, seismic moment release, radiated seismic energy, and so on (e.g., Ide et al., 2007; Ide & Yabe, 2014; Tan & Marsan, 2020; Yabe et al., 2019). Recent studies suggest that heterogeneities in the frictional properties on the fault control the distribution of events and their source characteristics (e.g., Baba et al., 2020; Nishikawa et al., 2019; Obara et al., 2010; Takemura et al., 2019; Tanaka et al., 2019).

The event size distribution is one of the scaling relationships that characterize the source processes of seismic phenomena. Ordinary earthquakes follow the Ishimoto-Iida or Gutenberg-Richter (GR) law (e.g., Gutenberg & Richter, 1944; Ishimoto & Iida, 1939), a power-law relationship implying that the source fault
is self-similar. The negative of the slope (the $b$-value) is commonly related to the stress state of the medium (Scholz, 1968, 2015). In contrast, volcanic tremor follow exponential-law size distributions (e.g., Benoit & McNutt, 2003), implying that the source process has a characteristic size. Most studies have shown that slow earthquakes follow a power-law size distribution (Bostock et al., 2015; Ito et al., 2009; Kao et al., 2010; Nakamura & Sunagawa, 2015; Staudenmaier et al., 2019; Wech et al., 2010), although some observations indicate that they follow an exponential-law size distribution (Chestler & Creager, 2017; Yabe & Ide, 2014).

A recent study of shallow tectonic tremor along the Nankai trough (Nakano et al., 2019) found that the event size distribution follows a tapered Gutenberg-Richter (TGR) distribution (Kagan, 2002), given by

$$
\Phi(M) = \left( \frac{M}{M_c} \right)^\beta \exp \left( \frac{M - M_c}{M_c} \right) \text{ for } M_c < M < \infty,
$$

where $M$ is seismic moment, $M_c$ is the catalog completeness threshold, and $M_c$ is the corner moment. $\beta$ controls the slope of the distribution; $\beta = 2b/3$ in the ordinary Gutenberg-Richter law. A TGR distribution may reconcile the contradictory findings of previous studies: power-law distributions better fit the overall size distribution, but exponential distributions may better fit the observations when only the largest events are observable. For ordinary earthquakes, the $b$-value of the GR law, and accordingly $\beta$, has been related to the stress level in the medium (Scholz, 1968, 2015), and the corner moment $M_c$ may be related to the fault dimension, which is specific to the causative fault (Kagan, 2002). For Nankai trough slow earthquakes, both $\beta$ and $M_c$ differ during different time periods in the same source region (Nakano et al., 2019), implying that the source characteristics of these events change with time, although the cause is poorly understood.

In this study, we analyzed the size distributions of shallow tectonic tremor along the Nankai trough during tremor episodes that occurred off the city of Kumano, Mie Prefecture, in 2016 and off the Kii Channel in 2018. By fitting the data with the TGR distribution, we found that the size distribution parameters of shallow tectonic tremor changed during the course of each episode, indicating that the source characteristics changed. We qualitatively interpreted the controlling factors of this distribution using the probabilistic cell automaton (PCA) model for slow earthquakes proposed by Ide and Yabe (2019). We found that the changes in the tremor event size distributions can be attributed to changes in the accumulated stress or the pore pressure on the fault.

### 2. Observed Changes of Tremor Size Distributions

#### 2.1. Estimation of Tremor Size Distribution

Using data obtained from the permanent Dense Oceanfloor Network System for Earthquakes and Tsunamis (DONET; Kaneda et al., 2015; Kawaguchi et al., 2015, Figure 1), we analyzed intensive tremor episodes with durations longer than a month; these include one that occurred off Kumano in April 2016, with a duration of about a month, and another off the Kii Channel that started in mid-February 2018 and continued for about 4 months (Figure 1). We referred to the seismic energy catalog of Nakano et al. (2019) for the 2016 off-Kumano activity, and for this study we estimated the radiated seismic energy of tremor events during the 2018 off-Kii Channel activity.

We estimated tremor energy by the method of Nakano et al. (2019). We first determined tremor source locations by the envelope correlation method (Ide, 2010; Obara, 2002). We used the daily average of these locations (Figure S1) for energy estimations because of their large scatter, which may be due to strong heterogeneities in velocity structures in the accretionary prism (Takeura et al., 2020). We next computed the energy rate waveforms at the source from three-component seismograms that were band-pass filtered between 2 and 8 Hz and corrected for the site amplification factors given by Yabe et al. (2021). We defined a tremor event as one in which the seismic energy rate continuously exceeded a threshold of $10^7$ J/s. Nakano et al. (2019) tried thresholds ranging between $10^7$ and $10^8$ J/s and found that they do not affect the nature of the size distributions. The seismic energy of each tremor event was then obtained by integrating the energy rate waveform over the time during each event. As the seismic energy of the tremor signal is proportional to the seismic moment (Ide & Yabe, 2014; Yabe et al., 2019), we used these seismic energy estimates to
represent the tremor event size. Signals from ordinary earthquakes were removed by reference to the catalogs of the Japan Meteorological Agency and U.S. Geological Survey.

To investigate the changes in event size distributions during each tremor episode, we fitted the TGR distribution given by Equation 1 to the size distributions obtained from sliding 10-day time windows (Figure 2). We assumed a catalog completeness magnitude $M_c$ of $3.0 \times 10^4$ J.

![Figure 1](image1.png)

**Figure 1.** (a) Map showing locations of DONET stations (triangles) and 10-day average locations of tectonic tremor events (circles). Dark gray triangles indicate DONET stations used in this study. Colors of circles represent the slope ($\beta$) of the size distribution of tremor events (10-day averages). (b) Longitudinal distribution of $\beta$. Error bars indicate the standard error of $\beta$ values.

![Figure 2](image2.png)

**Figure 2.** Size distributions of tectonic tremor during successive 10-day sliding time windows for (a) the 2016 off-Kumano episode and (b) the 2018 off-Kii Channel episode.
2.2. Changes of Tremor Size Distributions

Figure 3 shows how the size-distribution parameters $\beta$ and $M_c$ of the tremor size distributions changed with time for the 2016 off-Kumano and 2018 off-Kii Channel tremor episodes; $\beta$ increased and $M_c$ decreased near the end of the 2016 episode and in the middle and end of the 2018 episode. The change was also clear in the event size distributions of successive 10-day time windows (Figure 2). Because the tremor source migrated during each episode (Figure S1), we plotted the distributions of $\beta$ and $M_c$ in Figure 1 and Figure S2, respectively, at positions representing the 10-day average of tremor source locations. In the 2016 off-Kumano episode, higher $\beta$ values with lower $M_c$ were concentrated at the southeast end of the source area. In the 2018 off-Kii Channel episode, the activity was mainly concentrated between longitude 135.0°E and 135.5°E, and both $\beta$ and $M_c$ showed distinct variations in this area. We note that these estimations were from tremor events scattered within 10–20 km of the average location. These results imply that the changes in the size-distribution parameters may be caused by spatial or temporal changes in the source characteristics of the tremor events.

3. Size Distribution of Slow Earthquakes Expected from the 2D PCA Model

3.1. 2D PCA Model

We investigated the cause of the observed changes in the tremor event size distributions by using the 2D PCA model of slow earthquakes proposed by Ide and Yabe (2019), which is an extension of the 1D Brownian slow earthquake model (Ide, 2008) to a 2D source fault. This model has successfully reproduced various scaling relationships of slow earthquakes, including their TGR-like event size distributions. In the 2D PCA model, the fault plane of a slow earthquake is divided into $N_x \times N_y$ cells, and each cell has two states: “stop” and “slip.” The state of each cell is updated stochastically according to the states of neighboring cells: Each “stop” cell becomes a “slip” cell with a probability $N_k p_s$, where $N_k$ is the number of surrounding cells in the “slip” state and $p_s$ is a probability of interactions between adjacent cells, and each “slip” cell becomes a “stop” cell with a probability $4- N_k p_s$. In addition, Ide and Yabe (2019) introduced the random ignition of slip in a cell with a probability $p_l$, which may be related to the slow loading from the surrounding medium. They also considered energy dissipation during slip, which suppresses slip in the cell with a probability $p_v$, introducing an additional characteristic scale to the event size distribution. The status of each cell ($\nu^i$) is updated based on...

Figure 3. Temporal changes of event number and the slope $\beta$ and corner moment $M_c$ of the tremor size distributions obtained from 10-day sliding time windows during the (a) 2016 off-Kumano and (b) 2018 off-Kii Channel episodes. Vertical bars represent uncertainties on $\beta$ and $M_c$. 
\( v_i^{k+1} = H \left( v_i^k + p_b \sum_{NN} (v_j^k - v_i^k) + p_l - p_v v_i^k - \xi \right) \),

(2)

where \( NN \) represents the four nearest neighbor cells, \( H() \) is the Heaviside function, \( i \) and \( k \) represent the cell number and time step, respectively, and \( \xi \) is a random number with a uniform distribution between 0 and 1 (Ide & Yabe, 2019). The value of \( v_i^k \) is 0 in the “stop” state and 1 in the “slip” state.

3.2. Dependence of Tremor Size Distribution on Probability Parameters

We used the 2D PCA model to investigate the dependence of \( \beta \) and \( M_c \) for the tremor size distribution on each of the probability parameters for synthetic tremor. We simulated tremor events with a fixed source size \( Nx = Ny = 101 \) for \( 10^6 \) steps. The tremor event size was defined as the total number of slipped cells during a tremor event, which ends when the number of slipping cells becomes zero. The dependence on \( p_b \) was surveyed for tremor events computed with \( p_l = p_v = 0.0 \). The dependences on \( p_v \) and \( p_l \) were studied for fixed values of \( p_l = 0.0 \) and \( p_v = 0.01 \), respectively, with \( p_b = 0.1 \). We note here that \( p_l \) should be smaller than \( p_v \), otherwise the slipping cells proliferate without suppression (see Equation 2). Then we estimated the size-distribution parameters \( \beta \) and \( M_c \) by fitting the TGR distribution to the event size distributions synthesized by using each combination of the probability parameters by setting \( M_t = 100 \) event size units. The event size distributions of the synthetic tremor computed by varying \( p_b \), \( p_l \), and \( p_v \) are shown in Figures S3, S4, and S5, respectively.

Figure 4 shows the dependence of \( \beta \) and \( M_c \) values for each probability parameter of the 2D PCA model. When the ignition probability \( p_l \) increases, the slope \( \beta \) of the size distribution decreases while the corner event size \( M_c \) increases. The anticorrelation of \( p_l \) and \( \beta \) is similar to the known anticorrelation between the b-value of the GR law and the stress level in the medium for regular earthquakes (Scholz, 1968, 2015). The dependence on the stopping probability \( p_v \) was opposite to the dependence on \( p_l \). This behavior is easily understood because these probability parameters have opposite signs in Equation 2. Energy dissipation during slip suppresses growth of the event, and accordingly the ratio of large events to small events decreases. This effect introduces an additional characteristic size to the system and accordingly reduces \( M_c \). The dependence on the probability \( p_b \) is rather complex. Both \( \beta \) and \( M_c \) increase as \( p_b \) increases for \( p_b < 10^{-3} \), whereas \( M_c \) decreases while \( \beta \) remains almost constant for \( p_b > 10^{-2} \). When \( p_b \) is too small, slip on a cell hardly propagates to surrounding cells and a slipping cell hardly stops, in which case the event size is mostly determined by the duration of slip at one cell. We do not expect such behavior for the source of short-term slow earthquake episodes. When \( p_b \) is large enough, slip on a cell easily propagates to surrounding cells and slip in a cell easily stops when it is surrounded by “stop” cells, which may reduce event durations and decrease \( M_c \) at the largest \( p_b \) values.
4. Discussion

In both of the tremor episodes we studied along the Nankai trough, $\beta$ increased as $M_c$ decreased in the later part of the episode as the rate of events decreased. These changes can be qualitatively explained in the 2D PCA model by a decrease in the event ignition probability $p_l$ or an increase in the energy dissipation probability $p_e$. In the following, we discuss the causes that may change these probabilistic parameters during slow earthquakes. Because the tremor sources migrated during each episode (Figure S1), the changes in these parameters may represent spatial or temporal changes in the source characteristics, and we consider physical properties on the source fault that cause either spatial or temporal changes of these probability parameters.

The main factors that control slow earthquake activity are the stiffness of the host rock, stress accumulation, and frictional resistance on the fault interface. Host rock stiffness may control the interactions of fault slip with the local surroundings, which was modeled as the probability $p_l$ in the 2D PCA model, but cannot explain the observed changes of the tremor size distributions.

Accumulated stress on the causative fault drives the spontaneous activity of regular and slow earthquakes (e.g., Matsuzawa et al., 2010). Accumulated stress that is initially high is released gradually in slow earthquakes. This change may decrease the event ignition probability $p_l$ that is consistent with the observed $\beta$ increase and $M_c$ decrease in the later part of tremor episodes. Because the slip history of previous slow earthquakes may result in a spatially heterogeneous distribution of accumulated stress (e.g., Matsuzawa et al., 2010), the migration of tremor sources may also affect the tremor size distributions. It is challenging to estimate the stress accumulation on a source fault before an event occurs; however, the degree of coupling between the overriding and subducting plate may affect the stress accumulation rate and accordingly the slip ignition probability. The coupling ratio on the plate interface has been found to be spatially heterogeneous along the Nankai trough (Nishimura et al., 2018; Noda et al., 2018; Yokota et al., 2016) and is inversely correlated with slow earthquake activity (Baba et al., 2020; Takemura et al., 2019). Hence, spatial variations of the coupling ratio may also be related to the variations of the event size distributions.

Frictional resistance depends on the pore-fluid pressure on the fault interface. Because an increase in pore-fluid pressure reduces the normal stress and accordingly the frictional resistance, pore fluid is considered a primary trigger of slow earthquakes (e.g., Kato et al., 2010; Obara, 2002). Theoretical studies modeling slow earthquakes have assumed that pore fluid reduces the normal stress on the fault (e.g., Gao & Wang, 2017; Liu & Rice, 2007; Matsuzawa et al., 2010). A decrease in pore-fluid pressure increases frictional resistance during slip and therefore increases the energy dissipation probability $p_e$ or decreases the slip ignition probability $p_l$ in the 2D PCA model. The observed $\beta$ increase and $M_c$ decrease can be explained by a decrease of pore-fluid pressure as tremor activity decreases in the later part of tremor episodes.

The excess pore-fluid pressure inferred from low shear-wave velocity anomalies in the accretionary prism has been correlated with the distribution of shallow VLFEs along the Nankai trough (Kitajima & Saffer, 2012; Tonogawa et al., 2017). Recent studies have detected along-dip and along-strike variations of tremor and VLFE activities, implying that heterogeneous frictional properties on the plate interface affect slow earthquake activity (Nishikawa et al., 2019; Tanaka et al., 2019; Yabe et al., 2019, 2021). The spatially heterogeneous distribution of pore-fluid pressure and frictional properties on the fault interface may change the event size distribution of tremor as it migrates. At shallow depths, the frictional properties of clay gouge produce velocity-strengthening behavior when water is included in minerals’ interlayers (Ikari et al., 2007). Clay minerals become dehydrated at depths greater than 8 km by the increased temperature and pressure, and the resulting fluid may exist in pore spaces rather than in the clay minerals (Ikari et al., 2007). The dehydration depth is close to the source depths of VLFEs along the Nankai trough (Nakano et al., 2018; Sugioka et al., 2012). Since VLFEs and tectonic tremor are the same phenomena but observed in different frequency ranges (Kaneko et al., 2018; Masuda et al., 2020), depth-dependent frictional properties may also affect the event size distribution of tectonic tremor.

Seismic observations have detected migrations of pore fluid coincident with slow earthquakes (Gosselin et al., 2020; Kano et al., 2019; Nakajima & Uchida, 2018; Warren-Smith et al., 2019; Zal et al., 2020), implying that pore-fluid pressure on the fault changes during a tremor episode. Tidal stress changes also affect normal stress and thereby tremor activity (e.g., Ide & Tanaka, 2014), but we can ignore this effect because the changes we detected in size distribution parameters occurred in time windows 10 days long.
In this study, we interpreted observed changes in the size distributions of tectonic tremor based on the 2D PCA model. The slope $\beta$ expected from the 2D PCA model is usually 0.5, a value that is smaller than the observed values except for the largest $p_i$ values. Although the 2D PCA model reproduces certain statistical characteristics of slow earthquakes, such as duration-moment scaling and TGR size distribution, there remains room for improvement. For example, the 2D PCA model only considers interactions with the nearest neighboring cells and ignores interactions with more distant cells. It also does not include the effects of slip history, which are necessary to reproduce lateral migrations over long distances. Therefore, the interpretations in this study are still qualitative. Further improvement of data analysis and theoretical models is needed to improve our understanding of the source process of slow earthquakes.

5. Conclusions

Shallow tectonic tremor along the Nankai trough follow the tapered Gutenberg-Richter distribution (Kagan, 2002), a power-law distribution of event sizes with an exponential taper for the largest events. In our study of temporal changes of the event size distribution of shallow tectonic tremor during long tremor episodes off Kumano in 2016 and off the Kii Channel in 2018, we found that the slope of the event size distribution increased while the cut-off magnitude decreased in the later part of each episode. The 2D PCA model of slow earthquakes (Ide & Yabe, 2019) allowed us to interpret the observed changes in the tremor size distribution qualitatively by a decrease in the probability of slip ignition on the fault or an increase in energy dissipation during slip. These changes can be attributed to the release of accumulated stress by slow earthquakes or spatial-temporal variations of pore-fluid pressures during slow earthquakes.

Data Availability Statement

Seismic waveform data from DONET can be downloaded from http://www.hinet.bosai.jp/?LANG=en (National Research Institute for Earth Science and Disaster Resilience, 2019). The earthquake catalog of the Japan Meteorological Agency can be downloaded from http://www.data.jma.go.jp/svd/eqev/data/bulletin/hypo.html. The earthquake catalog of the United States Geological Survey can be downloaded from https://earthquake.usgs.gov/earthquakes/search/. The authors thank two anonymous reviewers and the Editor G. Prieto for careful review and constructive comments, which have improved the manuscript.

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