An Unsupervised Learning Approach for Spectrum Allocation in Terahertz Communication Systems

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Abstract—We propose a new spectrum allocation strategy, aided by unsupervised learning, for multiuser terahertz communication systems. In this strategy, adaptive sub-band bandwidth is considered such that the spectrum of interest can be divided into sub-bands with unequal bandwidths. This strategy reduces the variation in molecular absorption loss among the users, leading to the improved data rate performance. We first formulate an optimization problem to determine the optimal sub-band bandwidth and transmit power, and then propose the unsupervised learning-based approach to obtaining the near-optimal solution to this problem. In the proposed approach, we first train a deep neural network (DNN) while utilizing a loss function that is inspired by the Lagrangian of the formulated problem. Then using the trained DNN, we approximate the near-optimal solutions. Numerical results demonstrate that comparing to existing approaches, our proposed unsupervised learning-based approach achieves a higher data rate, especially when the molecular absorption coefficient within the spectrum of interest varies in a highly non-linear manner.

Index Terms—Terahertz communication, machine learning, unsupervised learning, spectrum allocation, adaptive bandwidth

I. INTRODUCTION

Terahertz (THz) communication (THzCom) has been envisioned as a key wireless technology in the sixth-generation (6G) and beyond era [1]. The THz band has enormous potential to support tera-bits-per-second (Tbps) data rates and massive connections in 6G networks, due to the tens up to a hundred GHz bandwidth [2]. Thanks to the recent advancements in manufacturing THz transceivers and antennas, as well as the experimental licenses (95 GHz–3 THz) opened by the US Federal Communications Commission, increasing endeavors have been devoted to the design and development of practical THzCom systems over the past few years [3, 4].

Despite the promise, THzCom encounters unique challenges that are different from those experienced at lower frequencies, e.g., severe spreading loss, higher channel sparsity, and the unique molecular absorption loss [5]. The molecular absorption loss is frequency-dependent, divides the whole THz band into several ultra-wide transmission windows (TWs), and introduces substantially varying distance-dependent path loss within TWs. These challenges need to be wisely tackled for developing practical THzCom systems.

The multi-band-based spectrum allocation is envisioned as one promising solution to supporting micro- and macro-scale THzCom systems, since it can effectively assign spectral resources when the variation in molecular absorption loss among the users in multiuser systems is very high [2]. In this allocation, the spectrum of interest is divided into non-overlapping sub-bands, and the sub-bands are utilized to support the users in the system.

Although different designs have been proposed to optimize the performance of multi-band-based spectrum allocation, e.g., [6–9], they all considered the spectrum of interest is divided into sub-bands with equal bandwidth. It is noted that the consideration of equal sub-band bandwidth (ESB) can lead to high variation in the channel quality levels among the users that are assigned to sub-bands. Different from ESB, adaptive sub-band bandwidth (ASB), where the spectrum of interest is divided into sub-bands with unequal bandwidths, can effectively reduce this variation, by allowing to change the bandwidth of sub-bands. Specifically, ASB allows the users that are assigned to the sub-bands in the edge and center regions of the THz TWs to occupy larger and smaller bandwidth, respectively, as compared to what would have been allocated when ESB is considered, thereby leading to an overall improvement in the data rate performance.

Motivated by the benefits, the multi-band-based spectrum allocation with ASB was first proposed in our previous studies [10, 11]. We note that the designs in [10, 11] are only applicable when the molecular absorption coefficient within the to-be-allocated spectrum is simple such that it can be modeled as a piecewise exponential function of frequency with minimal approximation errors. In many spectrum regions within the THz band, the molecular absorption coefficient varies in a highly non-linear manner; thus, it cannot be modeled as a piecewise exponential function of frequencies in such spectrum regions. It follows that the designs in [10, 11] cannot be adopted in such spectrum regions. This motivates the current work.

In the current work, we study multi-band-based spectrum allocation with ASB to improve the spectral efficiency of THzCom systems. We formulate an optimization problem to determine the optimal sub-band bandwidth and optimal transmit power. We then propose an unsupervised learning-based ap-
proach to obtaining a near-optimal solution to the formulated optimization problem. In the proposed approach, we first train a deep neural network (DNN) where a loss function inspired by the Lagrangian of the formulated optimization problem is used. Thereafter, using the trained DNN, we approximate the near-optimal solution to the formulated optimization problem. Using numerical results, we demonstrate that when the values of the molecular absorption coefficient within the spectrum of interest can be modeled as an exponential function of frequency, the data rate obtained by our proposed unsupervised learning-based approach converges to the optimal data rate achieved by the existing spectrum allocation approach with ASB. We also demonstrate that when the values of the molecular absorption coefficient within the spectrum of interest change rapidly and thus cannot be modeled as an exponential function of frequency, our proposed unsupervised learning-based approach outperforms the existing approach.

Notations: Matrices and column vectors are denoted by uppercase and lowercase boldface symbols, respectively. Scalar variables are denoted by italic symbols. Given a matrix $A$, $A_r$ denotes the $r$th row vector of $A$. Given a column vector $a$, $a^T$ and $a_r$ denote the transpose and the $r$th element of $a$, respectively. Moreover, $I_m$ and $L_m$ denote $m \times m$ identity matrix and $m \times m$ lower triangular matrix with all non-zero values as 1, respectively. Furthermore, $I_n$ denotes the $m \times 1$ vector with all entries as 1. The curled inequality symbols, e.g., $\langle$, denote generalized inequalities, i.e., componentwise inequality between vectors.

II. SYSTEM MODEL AND PROBLEM FORMULATION

We consider a three-dimensional (3D) indoor THzCom system where the high data rate demands of $n_1$ users are supported by a single AP. We consider that the users are stationary and distributed uniformly on the floor in the indoor environment. We denote $d$ as the $n_1 \times 1$ communication distance vector of the AP-user channels. For notational convenience, we consider that the elements in $d$ are ordered such that $d_1 < d_2 < \cdots < d_{n_1}$.

A. THz Spectrum

1) Spectrum of Interest: We define the regions which generally exhibit an decreasing and increasing molecular absorption coefficient behaviour within an ultra-wideband THz TW as the negative absorption coefficient slope region (NACSR) and the positive absorption coefficient slope region (PACSR), respectively, as depicted in Fig. 1 [10]. It is noted that at the THz band, the available bandwidths in each NACSR and PACSR are in the order of tens of GHz [10, Table 1]. Considering this, we focus on the scenario where the to-be-allocated spectrum of interest fully exists in either an NACSR or a PACSR of a THz TW in this work. Without loss of generality, in the rest of the paper, we present spectrum allocation in an NACSR only since this spectrum allocation can be easily applied to a PACSR.

We focus on multi-band-based spectrum allocation with ASB. Thus, we divide the spectrum of interest into $n_S$ sub-bands that are of unequal bandwidths. We denote $b$ and $f$ as the $n_S \times 1$ vectors of the bandwidth and the center frequency of the sub-bands, respectively. For notational convenience, we label the sub-bands such that $f_1 < f_2 < \cdots < f_{n_S}$, as shown in Fig. 1. Thus, we have

$$f_s = \epsilon_f + \frac{1}{2} \sum_{k=1}^{s-1} (b_k + 1) \epsilon_s = \mathbf{A}_s \mathbf{b} + \epsilon_f,$$

(1)

where $s \in \{1, 2, \cdots, n_S\}$ and $\epsilon_f$ is the start frequency of the spectrum of interest, as shown in Fig. 1. Here, $\mathbf{A}$ is an $n_S \times n_S$ matrix with $\mathbf{A} = \mathbf{I}_{n_S} - \frac{1}{2} \mathbf{I}_{n_S}$. Considering this, we have $\mathbf{f} = \mathbf{A} \mathbf{b} + \mathbf{1}_{n_1} \epsilon_f$. Due to the consideration of ASB, we have

$$0 \leq \mathbf{b} \leq b_{\text{max}},$$

(2)

where $b_{\text{max}}$ denotes the upper bound on bandwidth of the sub-band. We then denote $b_{\text{tot}}$ as the total available bandwidth within the spectrum of interest and express it as

$$b_{\text{tot}} = \mathbf{1}_{n_1} b.$$

(3)

2) Sub-band Assignment: In the considered system, we assume that the users in the system are served by separate sub-bands. This assumption is made to (i) ensure the data transmission to be free of intra-band interference (Intra-BI) and (i) eliminate the signal processing overhead and hardware complexity caused by frequency reuse in the system, which is also adopted in [6–8, 10, 11]. Considering this assumption, we set the total number of sub-bands within the spectrum of interest to be equal to the total number of users in the system, i.e., $n_S = n_1$. Also, following [6, 8, 9], we adopt distance-aware multi-carrier (DAMC)-based sub-band assignment to

To fully utilize the potentials of the huge available bandwidths at the THz band, it would be more beneficial to focus on resource allocation when the to-be-allocated spectrum of interest spans across multiple NACSRs and/or PACSRs. This consideration will be addressed in our future work.
improve the throughput fairness among users. The DAMC-based sub-band assignment assigns (i) the sub-bands with high absorption coefficients to the users with shorter distances and (ii) the sub-bands with low absorption coefficients to the users with longer distances.

B. Achievable Data Rate

We denote \( r \) as the \( n_S \times 1 \) rate vector of users. Considering spreading and molecular absorption losses experienced by THz signal propagation, we obtain the rate achieved in the \( s \)th sub-band as [12]

\[
 r_s = \int_{f_s - \frac{1}{2} b_s}^{f_s + \frac{1}{2} b_s} \log_2 \left( 1 + \frac{p_s \varrho e^{-k(f)d_s}}{f^2 d_s^2 b_s} \right) \, df, \tag{4}
\]

where \( \varrho \triangleq G_A G_U N_0^{-1} \left( \frac{c}{4\pi} \right)^2, \) \( G_A \) and \( G_U \) are the antenna gains at the AP and users, respectively, \( N_0 \) is the noise power density, \( c \) is the speed of light, and \( k(f) \) is the molecular absorption coefficient at \( f \). Furthermore, \( p_s \) denotes the \( n_S \times 1 \) transmit power vector.

In this work, we focus on the line-of-sight (LoS) rays of THz signals since the non-line-of-sight (nLoS) rays at the THz band are significantly attenuated due to high scattering and reflection losses [10–13]. Also, we omit the impact of fading in the THz channel as the prior studies at the THz band [10–13]. Moreover, following [6–9, 11], we omit the impact of blockages in this work. Finally, the impact of inter-band interference (Inter-BI) is not considered in this work since prior studies have proposed designs to suppress IBI with minimal throughput degradation [14].

C. Optimal Spectrum Allocation

We now design an efficient spectrum allocation strategy to harness the potential of the THz band. To this end, we study spectrum allocation with ASB to maximize the achievable data rate under given sub-band bandwidth and power constraints. Mathematically, this problem is formulated as

\[
P^o : \max_{p, b} \quad \mathcal{E}(d, p, b) \tag{5a}
\]

s. t. \quad \mathbf{1}_{n_S}^T p \leq p_{\text{tot}}, \tag{5b}

\[0 \leq p \leq p_{\text{max}}, \tag{5c}
\]

\[\mathbf{1}_{n_S}^T b = b_{\text{tot}}, \tag{5d}
\]

\[0 \leq b \leq b_{\text{max}}. \tag{5e}
\]

In \( P^o \), \( \mathcal{E}(d, p, b) \) is the objective function of the considered data rate maximization strategy. In this work, we consider proportional-fair data rate maximization, which leads to \( \mathcal{E}(d, p, b) = \mathbf{1}_{n_S}^T \log(r) \). Moreover, (5b) and (5c) are the power budget at the AP and the upper bound on the power allocated to each user, respectively. Furthermore, the justifications on (5d) and (5e) are given by (3) and (2), respectively.

3Consideration of nLoS rays, fading, blockages, and IBI can lead to a more accurate characterization of the considered THzCom system, which will be considered in our future works.

We note that it is extremely difficult, if not impossible, to analytically solve \( P^o \) using the traditional optimization techniques [15]. This is due to the difficulty in obtaining a tractable expression for \( r_s \) in terms of the design variables \( b \). On one hand, obtaining \( r_s \) as per (4) involves an integral, the limits of which depend on \( b \). On the other hand, the values of \( k(f) \) for all frequencies within the spectrum of interest are required to obtain \( r_s \). However, there does not exist a tractable expression that maps \( f \) to \( k(f) \) for all spectrum regions within the THz band. To tackle these challenges, we resort to unsupervised learning to obtain near-optimal solution to \( P^o \) [16, 17], and present the solution in Section III.

III. UNSUPERVISED LEARNING-BASED SOLUTION

In this section, we present an unsupervised learning-based approach to solving problem \( P^o \) in (4). In this approach, we first employ an offline training phase to train a DNN, utilizing (i) a loss function which is inspired by the objective function of the dual problem of \( P^o \) and (ii) a batch of realizations of distance vectors. Thereafter, during the implementation phase, we use the trained DNN to approximate the optimal solution to \( P^o \) for the given distance vector. Next, we will discuss the architecture of the adopted DNN in Section III-A, and the unsupervised learning model used in the training phase in Section III-B.

A. Architecture of DNN

The general architecture of the adopted DNN is presented in Fig. 2. The DNN consists of \( L \) fully-connected layers with multiple neurons in every layer. Each neuron in the network contains a linear operation, which is followed by a point-wise nonlinearity, also known as an activation function. Considering this, the output of the network, \( y \), is expressed as a non-linear function to the input of the network, \( x \), which is given by

\[
y = \mathcal{N}(x, \Theta) = g^{(L)} \left( g^{(L-1)} \left( \cdots g^{(1)} (x) \right) \right). \tag{6}
\]

Here, \( \Theta = \{ \varpi^{(\ell)}, \beta^{(\ell)} | \ell \in \{1, 2, \cdots, L\} \} \), denotes the set of parameters (i.e., weights and biases) of the DNN, and \( \varpi^{(\ell)} \) and \( \beta^{(\ell)} \) are the weights vector and the bias of the \( \ell \)th layer, respectively. Also, we have

\[
g^{(\ell)} (\rho) = \sigma^{(\ell)} \left( (\varpi^{(\ell)})^T \rho + \beta^{(\ell)} \right), \tag{7}
\]
where \( \sigma^{(l)}(\cdot) \) is the activation function of the \( l \)th layer.

During the implementation phase, we provide \( d \) as the input to the DNN and obtain the output as the approximated values of the optimization variables of \( P^o \), which are denoted by \( \bar{p} \) and \( \bar{b} \). Therefore, we have

\[
\begin{align*}
x &= d \quad \text{and} \quad y = \begin{bmatrix} \bar{p} \\ \bar{b} \end{bmatrix}.
\end{align*}
\]

B. Unsupervised Learning Model

The block diagram representation of the unsupervised learning model used in the training phase is depicted in Fig. 3. The unsupervised learning model takes a batch of realization of the distance vector, \( B_d \), as the input, and delivers the trained \( \Theta \) as the output. We note that the unsupervised learning model iteratively updates \( \Theta \) to ensure the best mapping being obtained between \( B_d \) and the near-optimal solution to \( P^o \) for the given \( B_d \).

1) Loss Function: The loss function of the unsupervised learning model is inspired by the objective function of the dual problem of \( P^o \). Specifically, the dual problem of \( P^o \) is given by

\[
\begin{align*}
P_D^o : \max_{\lambda, \Gamma} & \quad \min_{p, b} \mathcal{L}_o \\
\text{s.t.} & \quad \mathcal{L}_o \leq 0,
\end{align*}
\]

where \( \mathcal{L}_o = \mathcal{L}_o(d, p, b, \lambda, \Gamma) \) is the Lagrangian of \( P^o \) given by

\[
\begin{align*}
\mathcal{L}_o &= -E(d, p, b) + \lambda_1 (1^T_{n_S} p - p_{hot}) + \lambda_2 (1^T_{n_S} b - b_{hot}) \\
&\quad + \Gamma_1^T (0 - p) + \Gamma_2^T (p - p_{\max}) + \Gamma_3^T (0 - b) + \Gamma_4^T (b - b_{\max}),
\end{align*}
\]

and \( \lambda = [\lambda_1, \lambda_2]^T \) and \( \Gamma = [\Gamma_1, \Gamma_2, \Gamma_3, \Gamma_4] \) are the Lagrange multipliers associated with the constraints of \( P^o \). In our unsupervised learning model, \( p \) and \( b \) are approximated as \( \bar{p} \) and \( \bar{b} \) using the DNN, respectively, which is parameterized by \( \Theta \). Considering this, the problem \( P_D^o \) can be regeneratted into the following variable optimization as

\[
\begin{align*}
P^o : \max_{\lambda} & \quad \min_{\Theta} \hat{\mathcal{L}} \\
\text{s.t.} & \quad (5b), (5d) \\
&\quad \lambda \geq 0,
\end{align*}
\]

where \( \hat{\mathcal{L}} = \hat{\mathcal{L}}(d, \bar{p}, \bar{b}) \) is given by

\[
\hat{\mathcal{L}} = -E(d, \bar{p}, \bar{b}) + \lambda_1 (1^T_{n_S} \bar{p} - p_{hot}) + \lambda_2 \left(1^T_{n_S} \bar{b} - b_{hot}\right).
\]

In (12), \( \hat{\mathcal{L}} \) is obtained as a simplified version of \( \mathcal{L}_o \) given in (10). This is because the satisfaction of constraints (5c) and (5e) can be guaranteed by carefully choosing appropriate activation functions for the neurons in the \( L \)th (or the output) layer of the DNN, e.g., \( \sigma^{(L)}(\cdot) = \vartheta \times S(\cdot) \), where \( S(\cdot) \) is the sigmoid function, and \( \vartheta \) and \( \vartheta = p_{\max} \) for the first and the second \( n_S \) neurons of the output layer, respectively.

We note that the optimal value of \( P_D^o \) might be a loose global lower bound on the optimal value of \( P^o \), since \( P^o \) is not a convex optimization problem. However, we also note that the design variables of \( P_D^o \) are approximated using a DNN in our unsupervised learning model. \( P_D^o \) aims to optimize the DNN parameters, \( \Theta \). Thus, it can be concluded based on the universal approximation theorem that the optimal value of \( \hat{\mathcal{L}} \) provides a tight lower bound on the optimal value of \( P^o \) [16, 17]. Based on this conclusion and considering that a batch of realization of \( d, B_d \), is used during the training phase, we define the loss function of the unsupervised learning model, \( J \). Specifically, for each realization of \( d \) in \( B_d \), we obtained the corresponding \( \hat{\mathcal{L}} \), and then derive \( J \) as the mean of \( \hat{\mathcal{L}} \) values. Mathematically, \( J \) is obtained as

\[
J = J(\Theta, \lambda) = \frac{1}{n_T} \sum_{d \in B_d} \hat{\mathcal{L}},
\]

where \( n_T \) is the total number of realization of \( d \) in \( B_d \). We then iteratively update \( \Theta \) and \( \lambda \) with the objective of minimizing \( J \) to arrive at the near-optimal solution to \( P^o \).

2) Updating \( \Theta \) and \( \lambda \): The DNN parameters, \( \Theta \), are updated according to

\[
\Theta^{(k+1)} = \Theta^{(k)} - \delta_\Theta \nabla_{\Theta^{(k)}} J^{(k)}
\]

\[
= \Theta^{(k)} - \frac{\delta_\Theta}{n_T} \sum_{d \in B_d} \left[ \nabla_{\Theta^{(k)}} \hat{\mathcal{L}} \right]_{\Theta=\Theta^{(k)}, \bar{p}=\bar{p}^{(k)}, \bar{b}=\bar{b}^{(k)}, \lambda=\lambda^{(k)}}
\]

where \( \delta_\Theta \) is the learning rate and \( \Psi^{(k)} \) is the \( k \)th iteration value of \( \Psi \), with \( \Psi \in \{ \Theta, J, \bar{p}, \bar{b}, \lambda \} \). Considering the chain
rule, we express $\nabla_{\Theta} \hat{L}$ in (14) as

$$\nabla_{\Theta} \hat{L} = \nabla \Theta \left[ \nabla_{\Lambda} \hat{L} \right]$$

(15)

In (15), $\nabla_{\Lambda} \hat{L}$ and $\nabla_{\Lambda} \hat{L}$ can be derived as

$$\nabla_{\Lambda} \hat{L} = -\nabla_{\Lambda} \tilde{\Theta}(d, \tilde{p}, \tilde{b}) + \lambda_1,$$  

(16)

and

$$\nabla_{\Lambda} \hat{L} = -\nabla_{\Lambda} \tilde{\Theta}(d, \tilde{p}, \tilde{b}) + \lambda_2,$$  

(17)

respectively. Note that in (16) and (17), it is impossible to analytically derive $\nabla_{\Lambda} \tilde{\Theta}(d, \tilde{p}, \tilde{b})$ and $\nabla_{\Lambda} \tilde{\Theta}(d, \tilde{p}, \tilde{b})$, respectively. Hence, we numerically calculate the values of $\nabla_{\Lambda} \tilde{\Theta}(d, \tilde{p}, \tilde{b})$ and $\nabla_{\Lambda} \tilde{\Theta}(d, \tilde{p}, \tilde{b})$ by using

$$\nabla_{\Lambda} \tilde{\Theta}(d, \tilde{p}, \tilde{b}) = \frac{\tilde{\Theta}(d, \tilde{p}, \tilde{b}) - \tilde{\Theta}(d, \tilde{p}, \tilde{b})}{\varepsilon \tilde{p}},$$

(18)

and

$$\nabla_{\Lambda} \tilde{\Theta}(d, \tilde{p}, \tilde{b}) = \frac{\tilde{\Theta}(d, \tilde{p}, \tilde{b}) + \varepsilon \tilde{b} - \tilde{\Theta}(d, \tilde{p}, \tilde{b})}{\varepsilon \tilde{b}},$$

(19)

respectively, where $\varepsilon$ is a very small positive number. We also note that in (15), $\nabla \Theta$ can be calculated as a function of $\Theta^{(k)}$ utilizing the chain rule.

As for the Lagrangian multiplier, $\lambda$, it can be updated according to

$$\lambda^{(k+1)} = \left[ \lambda^{(k)} + \delta_{\lambda} \nabla_{\lambda}^{(k)} J^{(k)} \right]^+,$$

(20)

where $\delta_{\lambda}$ is the learning rate. In (20), $\nabla_{\lambda} \hat{L}$ can be derived as

$$\nabla_{\lambda} \hat{L} = \left[ \frac{1}{\lambda} \tilde{p} - \beta_{\text{tot}} \right] \tilde{p} = \tilde{p}^{(k)} = \tilde{b}^{(k)}.$$

(21)

Finally, we note that based on (14) and (20), we can iteratively update $\Theta$ and $\lambda$ in the unsupervised learning model.

IV. CONVEX OPTIMIZATION-BASED SOLUTION FOR A SPECIAL CASE

As mentioned in Section III, it is impossible to analytically solve the spectrum allocation problem $\text{PO}$ using traditional optimization techniques for the generalized system model considered in this work. Despite so, for a special case of the considered system model, the solution to $\text{PO}$ can be obtained using the convex optimization theory and standard convex problem solvers [10, 11]. We next present this special case system and its solution using convex optimization, the performance of which will be used as a benchmark in Section V for demonstrating the effectiveness and benefits of our proposed approach in Section III.

In the considered special case system, the molecular absorption coefficient within the spectrum of interest, $k(f)$, can be modeled as an exponential function of frequency with minimal approximation errors. We note that there indeed exist PACSRs and NACSRs within the THz band where $k(f)$ can be modeled as an exponential function of frequency, e.g., between 0.771 and 0.821 THz, where the maximum modeling approximation error is 5%.

For the considered special case system, the data rate, $r_s$, can be approximated as a tractable expression in terms of $b$. Specifically, by modeling $k(f)$ within NACSRs as an exponential function of frequency, we can approximate $k(f)$ as $k(f) = e^{o_1 + o_2 f} + \eta_3$, where $\eta = [\eta_1, \eta_2, \eta_3]^T$ is the model parameter vector. This enables us to obtain $r_s$ as a tractable expression of $b$ as

$$r_s = b_s \log_2 \left( 1 + \frac{p_s |d_s| \tilde{e}(d_s + e_s f) + \delta_3}{b_s d_s^2 (A_s b + \epsilon f)^2} \right).$$

(22)

With the simplified expression $r_s$ in (22), and considering the substitution for $b$, given by $\tilde{b} = \tilde{b} + \tilde{b} \log(\hat{e} z)$, where $z$ is a new design variable vector that would replace $b$ in the optimization problem, and $\xi = [\xi_1, \xi_2, \xi_3]^T$ is a vector with real constants as its elements, the spectrum allocation problem for the special case system can be transformed into an equivalent standard convex problem given by

$$\tilde{P}_{\text{SC}}: \min \begin{cases} p_s \text{T} n_s \log(r) \end{cases} \quad \text{s. t.} \quad (5b), (5c), \quad \prod_{s=1}^{N_s} z_s^2 - z_{\text{tot}} \leq 0, \quad \text{z_min} \leq z \leq \text{z_max},$$

(23a)

$$z_{\text{tot}} = \left( \xi_3 - \xi_2 \epsilon_{\text{max}} - \xi_1 n_s \right) n_s, \quad \text{z_min} = \xi_3 - \epsilon_{\text{max}}, \quad \text{z_max} = \xi_3 - \epsilon_{\text{min}}.$$  

The transformed problem for the special case system, $\tilde{P}_{\text{SC}}$, can be solved efficiently by using standard convex problem solvers [15]. The details of the convex optimization-based approach can be found in our previous works in [10, 11].
On the other hand, general spectrum allocation problem considered in this work. AG can be modeled as an exponential function of frequency, i.e., in the generalized system investigated in Sections II and III.

The numerical results are obtained by considering a rectangular indoor environment of size 25 m × 25 m where an AP, which is located at the center of the ceiling of the indoor environment, serves 15 users. We consider the spectrum with a bandwidth of 50 GHz that exist in either (i) the NACSR sr,1 between 0.557 and 0.671 THz or (ii) the NACSR sr,2 between 0.752 and 0.868 THz is used to serve the users. We clarify that on hand, the molecular absorption coefficient, k(f), in sr,2 can be modeled as an exponential function of frequency with minimal approximation errors. Hence, the spectrum allocation problem in sr,2 is a special case of the general spectrum allocation problem considered in this work. On the other hand, k(f) in sr,1 cannot be modeled as an exponential function of frequency.

We implement the unsupervised learning model presented in Section III in Python. We utilize a five-layer DNN for the unsupervised learning model, which has 100, 100, 50, 25, and 30 neurons in the first, second, third, fourth, and fifth layers, respectively. The initial weights of the DNN are Gaussian random variables with zero mean and unit variance, and the initial biases are set to 0. The initial values of λ are set to a small constant of 0.1. The values of other system parameters, hyper-parameters of the unsupervised learning model, and the parameters of the convex optimization-based approach used for numerical results are summarized in Table I.

In Fig.4, we show the convergence of the proposed unsupervised learning-based approach when k(f) within the spectrum of interest can be modeled as an exponential function of frequency, i.e., considering the special case system investigated in Section IV. To this end, we plot the aggregated multiuser data rate, RAG, and total power and bandwidth constraints satisfaction when k(f) within the spectrum of interest cannot be modeled as an exponential function of frequency, i.e., in the generalized system investigated in Sections II and III.

V. NUMERICAL RESULTS

The numerical results are obtained by considering a rectangular indoor environment of size 25 m × 25 m where an AP, which is located at the center of the ceiling of the indoor environment, serves 15 users. We consider the spectrum with a bandwidth of 50 GHz that exist in either (i) the NACSR sr,1 between 0.557 and 0.671 THz or (ii) the NACSR sr,2 between 0.752 and 0.868 THz is used to serve the users. We clarify that on hand, the molecular absorption coefficient, k(f), in sr,2 can be modeled as an exponential function of frequency with minimal approximation errors. Hence, the spectrum allocation problem in sr,2 is a special case of the general spectrum allocation problem considered in this work. On the other hand, k(f) in sr,1 cannot be modeled as an exponential function of frequency.

We implement the unsupervised learning model presented in Section III in Python. We utilize a five-layer DNN for the unsupervised learning model, which has 100, 100, 50, 25, and 30 neurons in the first, second, third, fourth, and fifth layers, respectively. The initial weights of the DNN are Gaussian random variables with zero mean and unit variance, and the initial biases are set to 0. The initial values of λ are set to a small constant of 0.1. The values of other system parameters, hyper-parameters of the unsupervised learning model, and the parameters of the convex optimization-based approach used for numerical results are summarized in Table I.

In Fig.4, we show the convergence of the proposed unsupervised learning-based approach when k(f) within the spectrum of interest can be modeled as an exponential function of frequency, i.e., considering the special case system investigated in Section IV. To this end, we plot the aggregated multiuser data rate, RAG, and the value of 1Tn,b − phot obtained from the unsupervised learning-based approach in Figs. 4(a), 4(b), and 4(c), respectively, when the spectrum allocation problem is implemented in sr,2. We clarify that the values of 1Tn,p − pphot and 1Tn,b − bhot provide intuition to the satisfaction or the violation of the total power and bandwidth constraints, given in (5b) and (5d), respectively. Also, the value of RAG obtained from the convex optimization-based approach is plotted in Fig.4(a). We first observe from Fig.4(a) that for several initial iterations, the value of RAG obtained using the unsupervised learning-based approach is higher than that obtained using the convex optimization-based approach. This is due to the occasional violation of the constraints (5b) and (5d) that occur at corresponding initial iterations, which can be validated by observing 1Tn,p − pphot and 1Tn,b − bhot in Figs. 4(b) and 4(c), respectively. Moreover, after 200 iterations, we observe that the value of RAG obtained using the unsupervised learning-based approach converges to the optimal value obtained using the convex optimization-based approach, which shows the correctness of our proposed unsupervised learning-based approach. Finally, we observe from Figs. 4(b) and 4(c) that after 200 iterations, the values of 1Tn,p − pphot and 1Tn,b − bhot of the proposed unsupervised learning-based approach are very close to zero, which reflects that constraints (5b) and (5d) are satisfied when the proposed unsupervised learning-based approach is used.

We next show the convergence of the proposed unsupervised learning-based approach when k(f) within the spectrum of interest cannot be modeled as an exponential function of frequency.
frequency, i.e., considering the generalized system investigated in Sections II and III. To this end, we plot $R_{AG}$, $1_{n_{\text{tot}}} p - p_{\text{tot}}$, and $1_{n_{\text{tot}}} b - b_{\text{tot}}$ in Figs. 5(a), 5(b), and 6(c), respectively, when the spectrum allocation problem is implemented in $sr_{n1}$. We clarify that in $sr_{n1}$, $k(f)$ cannot be modeled as an exponential function of frequency with minimal approximation errors. However, for the sake of comparison, we obtain approximate solutions to the spectrum allocation problem in $sr_{n1}$ using the convex optimization approach while utilizing an inaccurate function of frequency with minimal approximation errors. We further observe that the value of $R_{AG}$ obtained using the unsupervised learning-based approach converges to a value higher than that obtained using the convex optimization-based approach. This is because when the convex optimization-based approach is used, where an exponential function with high approximation errors is used to model $k(f)$, only the sub-optimal $R_{AG}$ is obtained. This shows the significance of our proposed unsupervised learning-based approach, i.e., it gives much higher $R_{AG}$ for the spectrum allocation problem when $k(f)$ within the spectrum of interest cannot be modeled as an exponential function of frequency.

Finally, we plot $R_{AG}$ achieved by the spectrum allocation strategy with ASB [6–9] and the spectrum allocation strategy with ASB that is obtained from both convex optimization and unsupervised learning-based approaches, versus the upper bound on sub-band bandwidth, $b_{\text{max}}$, in Fig.6. We first observe that the proposed spectrum strategy with ASB achieves a significantly higher $R_{AG}$ compared to the strategy with ESB for different $b_{\text{max}}$, which demonstrates the benefits of our proposed strategy with ASB. Second, we observe that in $sr_{n1}$, the value of $R_{AG}$ obtained using the unsupervised learning-based approach converges to values higher than that obtained using the convex optimization-based approach for all $b_{\text{max}}$. This again shows the significance of our proposed unsupervised learning-based approach to obtain higher $R_{AG}$, especially when $k(f)$ within the spectrum of interest cannot be modeled as an exponential function of frequency.

VI. CONCLUSIONS

We investigated multi-band-based spectrum allocation with ASB for multiuser THzCom systems. We first formulated an optimization problem and then proposed an unsupervised learning-based approach to obtain near-optimal sub-band bandwidth and transmit power. In the proposed unsupervised learning-based approach, we first employed an offline training phase to train a DNN while utilizing a loss function inspired by the Lagrangian of the formulated problem. Then using the trained DNN, we approximated the near-optimal solutions to the optimization problem for the given distance vector. Using numerical results, we showed that when the values of the molecular absorption coefficient within the spectrum cannot be modeled as an exponential function of frequency, the data rate obtained by our proposed unsupervised learning-based approach outperforms that obtained by the existing convex optimization-based approach.

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