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Phys. Rev. Lett. 124, 106103 — Published 10 March 2020
DOI: 10.1103/PhysRevLett.124.106103
Meron Spin Textures in Momentum Space

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(Dated: February 19, 2020)

We show that a momentum-space meron spin texture for electromagnetic fields in free space can be generated by controlling the interaction of light with a photonic crystal slab having non-zero Berry curvature. These spin textures in momentum space have not been previously noted either in electronic or photonic systems. Breaking the inversion symmetry of a honeycomb photonic crystal gaps out the Dirac cones at the corners of Brillouin zone. The pseudo-spin textures of photonic bands near the gaps exhibit a meron or antimeron. Unlike the electronic systems, the pseudo-spin texture of the photonic modes manifests directly in the spin (polarization) texture of the leakage radiation, as the Dirac points can be above the light line. Such a spin texture provides a direct approach to visualize the local Berry curvature. Our work highlights the significant opportunities of using photonic structures for the exploration of topological spin textures, with potential applications towards topologically robust ways to manipulate polarizations and other modal characteristics of light.

Spin textures, the spin configuration in either real or momentum space, are of great interest in several subfields of physics. Skyrmion-related objects, including skyrmions, anti-skyrmions, merons, and anti-merons are topologically nontrivial spin textures. These textures have been extensively studied in various atomic and electronic systems such as Quantum Hall 2D electron gas, Bose-Einstein condensates, nematic liquid crystals and chiral magnets [1–7]. Antiskyrmions were discovered in tetragonal Heusler materials [8], while merons and antimerons in real space were discovered in chiral magnet thin film [9].

Since photons are massless spin-1 particles, skyrmion-related objects can also emerge as spin textures of photons [10, 11]. Real space skyrmions have been observed recently in surface plasmon polariton systems [11]. But there has not been any report of anti-skyrmions, merons and antimerons in optics. In this letter, using the honeycomb photonic crystal slab structure as shown in Fig. 1(a), we report meron and antimeron in momentum space. The existence of such objects has not been previously noted either in electronic or photonic systems. The observation of such spin textures may point to topologically robust ways to manipulate polarizations of light.

Skyrmion-related objects correspond to topologically nontrivial configurations of a three-component unit vector field \( \mathbf{n} = n_x \hat{x} + n_y \hat{y} + n_z \hat{z} \) distributed over a disk in a two-dimensional space with coordinates \((x, y)\) [12, 13]. They are all characterized by the topological skyrmion number

\[
Q = \frac{1}{4\pi} \int \mathbf{n} \cdot (\partial_x \mathbf{n} \times \partial_y \mathbf{n}) \, dx \, dy,
\]

The unit vector fields form a 2-sphere \( S^2 \). For skyrmions and antiskyrmions, one considers configurations where \( \mathbf{n} = \hat{z} \) at the center of the disk, and \( \mathbf{n} = -\hat{z} \) at its edge. (This is referred to as the “core-up” configuration.) Since the fields \( \mathbf{n} \) are the same at the edge, one can compactify the edge to a single point to form a sphere. These field configurations thus correspond to maps of \( S^2 \to S^2 \), which are characterized by the second homotopy group of the sphere \( \pi_2(S^2) = \mathbb{Z} \), with an integer topological number \( Q \) characterizing topologically distinct ways that the unit vectors wrap around the sphere. \( Q = +1 \) and \(-1 \) for skyrmions and antiskyrmions, respectively, for core-up configurations as discussed above. For core-down configurations, the signs are flipped, i.e. \( Q = -1 \) and \(+1 \) for skyrmions and antiskyrmions, respectively.

For merons and antimerons, one considers configurations where \( \mathbf{n} = \hat{z} \) at the disk center, \( \mathbf{n} \perp \hat{z} \) at its edge, and \( n_z \geq 0 \) over the whole disk. These field configurations correspond to maps of the disk to the upper hemisphere, with the disk edge imaged to the equator. With the following map:

\[
\mathbf{n} = (n_x, n_y, n_z) = (\sin \theta \cos \phi, \sin \theta \sin \phi, \cos \theta) \rightarrow \\
\mathbf{m} = (2n_x n_z, 2n_y n_z, 2n_z^2 - 1) = (\sin 2\theta \cos \phi, \sin 2\theta \sin \phi, \cos 2\theta)
\]

(2)

which maps a hemisphere to a sphere with \( 0 \leq \theta \leq \pi/2 \), \( 0 \leq \phi \leq 2\pi \), all the points on the equator of the hemisphere are mapped to the south pole of the sphere. Applying this map to the meron or anti-meron configuration results in a field configuration with \( \mathbf{m} = -\hat{z} \) on the edge of the disk. One can then repeat the same compactification process as the skyrmion case, and obtain an integer \( Q_m \) as the topological number for \( \mathbf{m} \). Since the continuous map from the \( \mathbf{n} \) field to the \( \mathbf{m} \) field doubles

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For merons and antimerons, one considers configurations where \( n_z = 0 \). Since the fields \( \mathbf{n} \) are the same at the edge, one can compactify the edge to a single point to form a sphere. These field configurations thus correspond to maps of \( S^2 \to S^2 \), which are characterized by the second homotopy group of the sphere \( \pi_2(S^2) = \mathbb{Z} \), with an integer topological number \( Q \) characterizing topologically distinct ways that the unit vectors wrap around the sphere. \( Q = +1 \) and \(-1 \) for skyrmions and antiskyrmions, respectively, for core-up configurations as discussed above. For core-down configurations, the signs are flipped, i.e. \( Q = -1 \) and \(+1 \) for skyrmions and antiskyrmions, respectively.

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the solid angle subtended, we have $Q_n = 2Q$. Therefore, merons and antimerons are characterized by half-integer skyrmion numbers: $Q = +1/2$ and $-1/2$ for core-up merons and antimerons, respectively; the signs are flipped for core-down merons and antimerons [14].

In addition to the topological number $Q$, skyrmion-related objects are further characterized by their polarity $p$ and vorticity $w$. $p = 1$ for $\mathbf{n} = \hat{z}$ and $p = -1$ for $\mathbf{n} = -\hat{z}$ at the center [15]. The vorticity $w$ indicates the rotation direction of the in-plane components of $\mathbf{n}$. Along a counter-clockwise loop around the center, for a given $w$, the in-plane components rotate an angle of $2\pi w$ counter-clockwise. Skyrmions and merons have $w = 1$; antiskyrmions and antimerons have $w = -1$.

Skyrmion-related objects can also emerge as spin textures of photons which are massless spin-1 particles [10, 11]. Consider a polarization state as characterized by a 2×2 density matrix $\rho$, with the basis being the right and left circularly polarized states $|\text{RCP}\rangle$ and $|\text{LCP}\rangle$. The Stokes parameters are defined as $S_i = \text{Tr}(\rho\sigma_i)$ where $\sigma_0 = I$; $\sigma_1 = \sigma_x$, $\sigma_2 = \sigma_y$, $\sigma_3 = \sigma_z$ are the Pauli spin matrices [16, 17]. For a pure polarization state $|\psi\rangle$, $S_0^2 = S_1^2 + S_2^2 + S_3^3$, thus its polarization is completely characterized by a three-component unit vector, also denoted as $\mathbf{n}$:

$$\mathbf{n} = (n_x, n_y, n_z) \equiv (S_1/S_0, S_2/S_0, S_3/S_0) \quad (3)$$

All $\mathbf{n}$’s form a unit 2-sphere known as Poincaré sphere. The Poincaré sphere of massless spin-1 photon is identical to the Bloch sphere of spin-$\frac{1}{2}$ electron [18].

**FIG. 1.** (a) A photonic crystal slab with a honeycomb lattice of circular air holes. The dielectric constant of the slab $\epsilon = 4$. The thickness of the slab is $d = 0.25a$, where $a$ is the lattice constant. The lower right shows the Brillouin zone. The wavevector $\mathbf{q} = (q_x, q_y)$ measured from $K$ and $K'$ are defined individually so that $q_y$ axis points towards $\Gamma$. (b) The band structure near $K(K')$. The two bands form a Dirac cone when $d_A = d_B = 0.22a$ (black dotted lines), while the degeneracy is lifted when $d_A = 0.18a, d_B = 0.26a$ (red). The blue dashed lines plot the fit from the effective Hamiltonian. (c) Pseudo-spin textures: core-up (down) meron for the lower (upper) band near $K$, and core-down (up) meron for the lower (upper) band near $K'$.

Here using photonic systems we show meron and antimeron spin textures in momentum space. We consider a photonic crystal slab consisting of a honeycomb lattice of circular air holes, where the holes at the two inequivalent sublattice sites are of different sizes [Fig. 1(a)]. For concreteness, the dielectric constant of the slab is $\epsilon = 4$, which approximates the dielectric constant of SiN at visible wavelengths.

The photonic band structure of the system exhibits a Dirac cone at $K$ and $K'$ when $d_A = d_B$ [black in Fig. 1(b)]. Breaking the inversion symmetry ($d_A \neq d_B$) gaps out the Dirac cone, resulting in two valleys at $K$ and $K'$ [19, 20] [red in Fig. 1(b)]. The system thus exhibits valley-contrastings physics similar to that in several two dimensional semiconductors [21, 22].

Breaking inversion symmetry induces meron pseudo-spin texture around $K$ and $K'$. In the vicinity of $K$ and $K'$, the system is described by an effective Hamiltonian as obtained using the $\mathbf{k} \cdot \mathbf{p}$ method [23–25]:

$$\hat{H}(q_x, q_y) = v_D(-q_y \hat{r}_x + q_x \hat{r}_y) + \Delta \hat{r}_z + \omega_0 \tau_0, \quad (4)$$

where the plus (minus) sign corresponds to $K(K')$. In this paper, $\mathbf{q} = (q_x, q_y)$ measures the difference of the wavevector from $K$ or $K'$, with $\hat{q}_y$ axis pointing towards $\Gamma$, and $\hat{q}_x = \hat{z} \times \hat{q}_y$, where $\hat{z}$ is the unit vector perpendicular to the slab (Fig. 1a). $\hat{\tau} = (\hat{r}_x, \hat{r}_y, \hat{r}_z)$ are the Pauli matrices of the pseudo-spin. $\mathbf{\tau}(\mathbf{q}) \equiv \langle \Psi(\mathbf{q})|\hat{\tau}|\Psi(\mathbf{q})\rangle = (\tau_x(q), \tau_y(q), \tau_z(q))$ defines the pseudo-spin texture with $|\Psi(\mathbf{q})\rangle$ being an eigenstate at $\mathbf{q}$. The basis of $\hat{\tau}$ is chosen such that $|\tau_z = \pm 1\rangle$ correspond to the even/odd states with respect to the $\hat{q}_y$ axis, and $|\tau_z = \pm 1\rangle$ correspond to the clockwise/anticlockwise-rotating states with respect to $\hat{z}$ [20, 25]. Below, we refer to the states $|\tau_z = +1\rangle$ and $|\tau_z = -1\rangle$ as the “up” and “down” pseudo-spin states, respectively. $v_D$ is the group velocity. The term with $\Delta$ breaks inversion symmetry and induces a bandgap of size $2|\Delta|$. $\omega_0$ is the speed of light in vacuum. $E(\mathbf{q})$ of the Hamiltonian in Eq. (4) (blue dashed lines) with fitting parameters $v_D = 0.26c, \Delta = -0.0056 \times 2\pi c/a, \omega_0 = 0.8646 \times 2\pi c/a$, where $c$ is the speed of light in vacuum. $E(\mathbf{q})$ agrees well with the numerically determined photonic bands near $K$ and $K'$ for the physical structure.

Figure 1(b) plots the eigenvalues $E(\mathbf{q})$ of the Hamiltonian in Eq. (4). At $K$ point ($\mathbf{q} = 0$), the pseudo-spin is up for the lower band and down for the upper band. Far away from $K$ point ($|\mathbf{q}| \gg |\Delta/v_D|$), the pseudo-plasms lie in the equatorial plane with vorticity $w = 1$. The pseudo-spin textures around $K$ are thus identified as core-up (core-down) meron for the lower (upper) band. Moreover, the in-plane pseudo-spin components $\langle \tau_x, \tau_y \rangle$ are locked at right angles with wavevector $(q_x, q_y)$. $\mathbf{\tau}(\mathbf{q})$ around $K$ and $K'$ are related: suppose a state in the lower band at $\mathbf{q}$ around $K$ has a pseudo-spin $(\tau_x, \tau_y, -\tau_z)$, the corresponding state in the lower band at the same $\mathbf{q}$ around $K'$ has a pseudo-spin $(\tau_x, \tau_y, \tau_z)$. The same mapping applies for the upper band. Therefore, the pseudo-spin textures around $K'$ are core-down (core-up) meron for the lower (upper) band. The meron pseudo-spin textures manifest the localized Berry curvature and the $\pm \pi$ Berry phase around $K$ and $K'$ [21].
We proceed to show that the meron pseudo-spin textures, and hence the local Berry curvature of the photonic bands, can be directly observed as the meron/antimeron spin texture of radiated photons. (Throughout the paper, the word "pseudo-spin" refers to the property of the modes in the photonic crystal slab, and the word "spin" refer to the polarization state of the outgoing radiation in free space.) In our system, the valleys are above the light line since \( \omega > 4\pi c/3a \). Consequently, unlike electronic systems, here the excited photonic modes will radiate out, and the leakage radiation carries information of the eigenmodes. Specifically, with respect to Fig. 1(a), suppose light is incident from the \( z < 0 \) side with the propagation direction indicated by a unit vector \( \hat{k} \). We define the S and P polarizations as having their electric field along the directions \( \hat{s} = \hat{z} \times \hat{k} \) and \( \hat{p} = \hat{z} \times \hat{k} \), respectively, and the right/left circular polarization (RCP/LCP) as having their electric fields along the directions \( \hat{r} = \hat{p} + i\hat{s} \) and \( \hat{l} = \hat{p} - i\hat{s} \), respectively, where we adopt the convention of \( \exp(-i\omega t) \). The conventions of the Poincaré sphere are chosen so that \( n_z = \pm 1 \) correspond to RCP/LCP, and \( n_x = \pm 1 \) correspond to P/S polarizations. Now we consider the map between pseudo-spin \( \tau \) of the eigenmode and spin \( n \) of the radiated photons. The radiation process can be described by a linear map \( \mathcal{F} : |\Psi\rangle \rightarrow |\Psi^{rad}\rangle \), where \( |\Psi\rangle \) are the internal states in the slab and \( |\Psi^{rad}\rangle \) are the corresponding leakage radiation. \( |\Psi\rangle \) can be expanded on the eigenbasis of \( |\tau_x = \pm 1\rangle \), which corresponds to even/odd states with respect to the \( g_y \) axis. The even/odd states radiate into P/S polarized states only, i.e. \( |\tau_x = 1\rangle \rightarrow |P\rangle \), \( |\tau_x = -1\rangle \rightarrow |S\rangle \), where the relative phase between |P\rangle and |S\rangle are fixed such that \( |\tau_z = 1\rangle \rightarrow |\text{RCP}\rangle \), \( |\tau_z = -1\rangle \rightarrow |\text{LCP}\rangle \) at the transmission side; consequently, \( |\tau_x = 1\rangle \rightarrow |\text{LCP}\rangle \), \( |\tau_x = -1\rangle \rightarrow |\text{RCP}\rangle \) at the reflection side. This map then induces a map between the pseudo-spin of photons in the slab and the spin of radiated photons as \( \mathcal{F}^{\star} : |\Psi^{rad}\rangle \rightarrow |\Psi^{rad}\rangle \), for transmission, \( \langle \tau_x, \tau_y, \tau_z \rangle \rightarrow \langle n_x, n_y, n_z \rangle \), for reflection, \( \langle \tau_x, \tau_y, \tau_z \rangle \rightarrow \langle n_x, -n_y, -n_z \rangle \). As a result, the meron pseudo-spin textures around \( K \) and \( K' \) can be directly observed as meron spin textures at the transmission side and antimeron spin textures at the reflection side.

In a typical optical experiment, the modes are excited by an externally incident beam. In order to use the measured polarization properties to infer the pseudo-spin properties of the photonic modes, it is important that the light being measured contains only the radiated photons from the modes, without any interference from direct reflection/transmission of the incident beam. Therefore, we propose the setup in Fig. 2(a), where we measure the polarization of light in high-order diffraction channels. Light with a specific frequency and polarization is incident on the sample at a specific angle to excite a desired photonic mode around one Brillouin zone corner \( (K_1) \). Due to the periodicity of the lattice, the excited mode radiates out to both 0th-order \( (K_1) \) and 1st-order \( (K_2 \text{ and } K_3) \) channels on both the transmission and reflection sides. Figs. 2(b-e) show the calculated 0th-order/1st-order reflection spectra for the RCP/LCP incident light with fixed parallel wavevector \( K_1 \). The 0th-order spectra in Figs. 2(b) and 2(c) exhibit Fano line shapes, superimposed upon a smoothly varying background corresponding to direct reflection [26]. This indicates strong interference between the directly reflected incident light and leakage radiation from the modes in the slab. In contrast, the 1st-order spectra in Figs. 2(d) and 2(e) exhibit resonances with Lorentzian line shapes, superimposed upon negligible background, indicating a negligible contribution from the direct reflection of the incident light. The wave amplitudes in these diffraction orders therefore arise entirely from the leakage radiation from the photonic mode in the slab. We emphasize that in this case, as long as the mode is excited, the polarization of the leakage radiation is independent of the polarization of the incident light.

In general we can selectively excite either the upper or the lower band with the use of different frequencies. Near the \( K \) point, where the difference in frequencies between the two bands is relatively small, we note that incident light with RCP (LCP) selectively excites the lower (upper) state [20] at \( K \) point, as shown in Fig. 2(d) and 2(e). In this case therefore we can in addition use different polarizations of the incident light to selectively excite the upper and lower band.

We now numerically study the polarization states of
FIG. 3. (a) Isofrequency contours of the lower band near $K$ point are studied frequency by frequency. (b-e) Stokes parameters as functions of $(q_x, q_y)$ at frequency $\omega = 0.855 \times 2\pi c/a$ which is in the lower band. (b) $S_0$ is the intensity of 1st-order reflected light. (c-e) Normalized Stokes parameters $S_1/S_0$, $S_2/S_0$ and $S_3/S_0$.

the photons in the 1st-order diffraction channel. The directions, frequencies and polarization of the incident light are chosen so that we probe the lower valley near $K$ point. At each frequency, we scan the incident parallel wavevectors $(k_x, k_y) = (K_{1x} + q_x, K_{1y} + q_y)$ around $K_1 = (1/\sqrt{3}, 1/3) \times 2\pi/a$, and calculate the four Stokes parameters from the electric fields of the 1st-order reflected light around $K_3 = (-1/\sqrt{3}, 1/3) \times 2\pi/a$ [Fig. 3(a)]. Figs. 3(b-e) plot the simulation results at the frequency $\omega = 0.855 \times 2\pi c/a$. Figure 3(b) shows the intensity distribution $S_0(q_x, q_y)$ of 1st-order reflected light in momentum space, where the bright peaks match the isofrequency contour of the lower band. Figure 3(c-e) show normalized Stokes parameters $S_1/S_0(q_x, q_y)$, $S_2/S_0(q_x, q_y)$ and $S_3/S_0(q_x, q_y)$, respectively. Since the Stoke parameters are not well defined for $S_0 = 0$, we only show results for $S_0 > 0.04$. The polarizations show significant variation in the direction along the isofrequency contour, but far less variation in the direction perpendicular to the contour. This is consistent with the fact that the spin texture of the leakage radiation manifests the pseudo-spin texture of the underlying photonic modes in this setup.

In Fig. 4, we plot the spin textures of the leakage radiation on the iso-frequency contours of the photonic band structure. Near the $K$-valley, for the reflected light in the 1st-order channel, the texture corresponds to a core-down antimeron with skyrmion number $Q = 1/2$, polarity $p = -1$ and vorticity $w = -1$ [Fig. 4(a)]. At the $K$ point, the spin points down ($\mathbf{n} = (0, 0, -1)$), corresponding to LCP. Away from the K-point the spin gradually rotates to the equatorial plane, corresponding to linearly-polarized light. Notice that the in-plane spin components on the circle around the $K$-point have a winding number of $-1$. At the $K'$-valley, the spin texture of the reflected light corresponds to a core-up anti-meron with $Q = -1/2, p = 1, w = -1$ [Fig. 4(b)]. This texture has the same winding characteristics as the texture shown in Fig. 4(a), but with spin up at the core of $K'$. For the transmitted light in the 1st-order channel, the texture corresponds to a core-up meron at $K'$ with $Q = 1/2, p = 1, w = 1$ [Fig. 4(c)], and a core-down meron at $K$ with $Q = -1/2, p = 1, w = 1$ [Fig. 4(d)]. Notice the in-plane spin components have a winding number of +1. The relation of spin textures between the transmitted and reflected lights can be explained by the mirror symmetry of the modes in the slab, whereas the relation of the textures between the $K$ and $K'$ valley can be explained by time-reversal symmetry and the adopted coordinate system. The observed spin texture of the leakage radiation corresponds well to the pseudo-spin texture of the photonic modes in the slab as described by Eq. (4). The analysis of the leakage radiation provides a direct visualization of the intriguing connection of spin, pseudo-spin, valley and band topology in the photonic valleytronic systems. In particular, our setup directly maps out the Berry curvature, which has only been probed indirectly by wave packet transport [27]. The spin texture for the leakage radiation as we observe here can manifest in a single electromagnetic pulse (and hence a single photon-wavefunction) [28].

In conclusion, we reveal the intrinsic meron pseudo-spin texture in momentum space in a photonic crystal slab, which can be directly observed as meron and antimeron spin texture by polarimetric study of high-order
diffracted light from the system. Such spin texture in momentum space has not been previously observed in either electronic or photonic systems. Our work indicates significant opportunities of using photonic structures to explore topologically non-trivial spin textures. Our result may also be important for arbitrary polarization generation [29–31]. For example, in this system, by changing the angle of incidence near the K point by a small amount, a wide variety of different polarizations can be generated.

This work is supported by the National Science Foundation (CBET-1641069).

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