CONTRIBUTION OF STELLAR TIDAL DISRUPTIONS TO THE X-RAY LUMINOSITY FUNCTION OF ACTIVE GALAXIES

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ABSTRACT

The luminosity function of active galactic nuclei has been measured down to luminosities \( \sim 10^{42} \) erg s\(^{-1}\) in the soft and hard X-rays. Some fraction of this activity is associated with the accretion of the material liberated by the tidal disruption of stars by massive black holes. We estimate the contribution to the X-ray luminosity function from the tidal disruption process. While the contribution depends on a number of poorly known parameters, it appears that it can account for the majority of X-ray selected AGN with soft or hard X-ray luminosities \( \lesssim 10^{43} - 10^{44} \) ergs s\(^{-1}\). If this is correct, a picture emerges in which a significant portion of the X-ray luminosity function of AGN is comprised of sources powered by tidal disruption at the faint end, while the sources at the bright end are powered by non-stellar accretion. Black holes with masses \( \lesssim 2 \times 10^6 M_\odot \) could have acquired most of their present mass by an accretion of tidal debris. In view of the considerable theoretical uncertainty concerning the detailed shape of the light curves of tidal disruption events, we focus on power-law luminosity decay (as identified in candidate tidal disruption events), but we also discuss constant accretion rate models.

Subject headings: accretion — black holes — cosmology: observations — galaxies: active — galaxies: nuclei

1. INTRODUCTION

A main-sequence or giant star passing near a massive black hole (MBH) of mass \( M_{bh} \lesssim 10^8 M_\odot \) is disrupted by the tidal forces \cite{Hills1975}. The disruption and the subsequent accretion of stellar debris by the black hole are potential powerful sources of X-ray emission \cite[e.g.,][]{MészárosSilk1977,Young1977,Rees1988,Rees1990}. The emission can be produced in various phases of tidal disruption, including the initial compression of the star \cite{Kobayashi2004}, the interaction of ejected debris with the ambient medium \cite{KhokhlovMelia1996}, in tidal stream collisions and debris fallback onto a nascent accretion disk \cite{Kochanek1994,lee1996,Kim1999,li2002}, and in the accretion of disk material onto the black hole \cite{Cannizzo1999,Ulmer1999}. The purpose of the present study is to estimate the contribution of activity associated with tidal disruptions to the luminosities of typical active galaxies.

Recently, surveys with HEAO 1, ASCA, Chandra, and XMM-Newton have yielded luminosity functions (LFs) of active galaxies at low and high redshift in the hard \cite[e.g.,][]{Ueda2003,Barger2005} and soft \cite[e.g.,][]{Hasinger2005} X-rays. The measured X-ray LFs extend to lower luminosities than their optical counterparts because contamination with host galaxy light makes optical detection of low-luminosity AGN difficult. The LFs are approximately broken power laws \( dN/d \log L_x \propto L_{x}^{\nu}(L_{x}+L_{x})^{-\mu} \) with \( \nu \approx -2 \) and \( -1 \lesssim \mu \lesssim 0 \) and \( L_x \sim 10^{43} - 10^{44} \) erg s\(^{-1}\). The power-law behavior at the bright end has been attributed to the intrinsic structure of quasar luminosity histories. The luminosity histories (light curves) are convolved with the black hole mass function to calculate the LF \cite[e.g.,][]{Wyithe2003,Hopkins2005}. The origin of the LF at the faint end, however, remains unknown.

At least a fraction of low-luminosity AGN must be powered by stellar tidal disruption. Here we estimate the contribution of these sources to the X-ray LF of AGN. This estimate is an essential step to understanding the origin of activity in AGN with black hole masses \( \lesssim 10^6 M_\odot \) and ultimately to understanding the origin of low-mass MBHs.

Theoretical investigations of the stellar tidal disruption process, and the detection X-ray flares that are candidate tidal disruption events \cite[e.g.,][]{KomossaGreiner1999,Komossa2004b,Halpern2004}, suggest that the nuclei in which stellar tidal disruption has occurred remain luminous for 1–10 yrs after disruption or longer. The integrated luminosity of the AGN depends on the mass of the stellar debris that remains bound to the black hole, and on the fraction of this mass that ends up accreting onto the black hole in a radiatively-efficient fashion. The bound mass can be a fraction \( f \sim 0.25 - 5 \) of the initial stellar mass \cite{Ayal2000}.

The bound mass inferred in the giant X-ray flare in NGC 5905 using a black-body fallback model is much smaller than the solar mass \cite{li2002}; in two other candidate flares, RX J1624.9+5554 and RX J1242.6–1119A, the light curves are consistent with masses \( \sim M_\odot \). \cite{Donley2002} constrained the rate of outbursts by comparing the ROSAT All-Sky Survey with archival pointed observations. They inferred a rate of \( \sim 10^{-3} \) yr\(^{-1}\) per galaxy. We adopt a theoretical estimate for the tidal disruption rate that is significantly higher (eq. \ref{eq:rate}).

The outline of our calculation of the AGN LF is as follows. In §1.1 we estimate the mass function of MBHs and the rate of tidal disruptions. In §2.2 we present simple models for the light curves of tidally disrupted stars. In §2.3 we calculate the LF and explore its dependence on various parameters in the model. In §3 we discuss implications of our estimate for the understanding of low-luminosity, X-ray selected AGN.

2. CALCULATION OF THE LUMINOSITY FUNCTION

2.1. Tidal Disruption Rate
Stars passing within distance \((\eta^2 M_{\text{bh}}/m_*)^{1/3} R_*)\) of the black hole, where \(m_*\) is the mass of the star, \(R_*\) is its radius, and \(\eta \sim 1\) is a numerical factor, are tidally disrupted. Here we estimate the tidal disruption rate in a galaxy with black hole of mass \(M_{\text{bh}}\) and stellar velocity dispersion \(\sigma\). The disruption rate depends on the detailed structure of the stellar nucleus of the galaxy. The galaxies relevant to this study are those with \(M_{\text{bh}} \lesssim M_{\text{max}} \approx 10^8 M_\odot (R_/R_\odot)^{3/2} (m_*/M_\odot)^{-1/2}\) which can disrupt stars.

In spheroids as faint as that of the Milky Way, the relaxation time within the black hole’s radius of dynamical influence \(r_{\text{bh}} \sim GM_{\text{bh}}/\sigma^2\) is short enough that a collisionally-relaxed distribution, \(\rho \propto r^{-\gamma}\), where \(\gamma \sim 1.5-1.75\), is set up (Bahcall & Wolf 1976, 1977; Merritt & Szell 2005). This is consistent with what is seen at the Galactic Center (Genzel et al. 2003; Schödel et al. 2006). But just beyond \(r_{\text{bh}}\), the Galactic Center density profile steepens to \(\rho \propto r^{-2}\), and this is also the slope observed with the Hubble Space Telescope near the centers of all but the most luminous galaxies (Gebhardt et al. 1996; Ferrarese et al. 2006). Furthermore, nuclear relaxation times in galaxies with \(M_{\text{bh}} \geq 10^7 M_\odot\) generally exceed a Hubble time (Faber et al. 1997) and so a Bahcall-Wolf cusp would not form.

The rate of stellar disruptions in stellar density cusps has been studied at various levels of detail (e.g., Frank & Rees 1976; Lightman & Shapiro 1977; Cohn & Kulsrud 1978; Magorrian & Tremaine 1999). We adopt the most recent estimate of the rate in a \(\rho \propto r^{-2}\) cusp (Wang & Merritt 2004)

\[
\Gamma(M_{\text{bh}}) \approx 7 \times 10^{-4} \, \text{yr}^{-1} \left(\frac{\sigma}{70 \, \text{km s}^{-1}}\right)^{7/2} \left(\frac{M_{\text{bh}}}{10^8 M_\odot}\right)^{-1} \times \left(\frac{m_*}{M_\odot}\right)^{-1/3} \left(\frac{R_*}{R_\odot}\right)^{1/4},
\]

where \(m_*\) and \(R_*\) are the mass and radius of the tidally disrupted stars.

The disruption rate in equation (1) must be weighted by the stellar mass function in the spheroid at distances from the black hole corresponding to the initial pericenter radii of tidally disrupted stars. These radii are typically similar to \(r_{\text{bh}}\) (Magorrian & Tremaine 1999). If the stellar mass function resembles the “universal” initial mass function (Kroupa 2001), the disruption is dominated by \(m_* \sim 0.1 M_\odot\) stars. However, the mass function near the black hole may differ from the universal initial mass function because higher-mass stars dynamically segregate closer to MBH, and because stars with an unusual initial mass function may form in situ near the MBH (e.g., Milosavljević & Loeb 2004 and references therein).

Mounting observational evidence indicates that the black hole mass and the velocity dispersion of the host spheroid are tightly correlated with best-fit relation \(M_{\text{bh}} \approx 1.7 \times 10^9 M_\odot (\sigma/200 \, \text{km s}^{-1})^{4.9}\) (e.g., Ferrarese & Ford 2005 and references therein). We explore departures from this fiducial relation by parameterizing the logarithmic slope of the relation \(M_{\text{bh}} \propto \sigma^4\).

No direct constraints on the cosmic density of MBH with masses \(\lesssim 10^7 M_\odot\) exist. The majority of these MBH should be in spiral galaxies. The density can be estimated by assuming a relation between the bulge luminosity and the black hole mass of the form \(L_{\text{bulge}} \propto A M_{\text{bh}}^2\). Following Ferrarese (2002), we substitute this in the Schechter LF \(\Phi(L) dL = \Phi_0(L/L_*)^\alpha e^{-L/L_*} dL/L_*\) to obtain a cosmic mass function of

\[
\Psi(M_{\text{bh}}) dM_{\text{bh}} = \Psi_0 \left(\frac{M_{\text{bh}}}{M_*}\right)^{(\alpha+1)-1} e^{-\left(M_{\text{bh}}/M_\odot\right)^{1/\beta}} dM_{\text{bh}}/M_*
\]

where \(\Psi_0 = k \Phi_\odot, M_* = (1.27 \beta (L_\odot/A)^{1/\beta})\), and \(\beta = L_{\text{bulge}}/L_\odot \approx 0.3\) for the Hubble type Sab (Simien & de Vaucouleurs 1986) which we use as reference. The latter is justified because spiral galaxies dominate galaxy LF below \(L_\odot\) (e.g., Nakamura et al. 2003). For the relation between the blue luminosity of the galaxy and the black hole mass we adopt \(L = 3900 L_{\odot} (M_{\text{bh}}/M_\odot)^{0.79}\) (Marconi & Hunt 2003).

The number density of \(\sim 10^5 M_\odot\) black holes estimated using equation (2) agrees with a similar estimate in Marconi et al. (2004), while the number density of \(\sim 10^3 M_\odot\) black holes exceeds their estimate by a factor \(\sim 3-4\). This may be a consequence of our using the \(B\)-band galaxy LF as reference, whereas Marconi et al. (2004) use the \(K\)-band LF that is flatter at the faint end. However our adoption of a steeper \(M_{\text{bh}}-\sigma\) relation than they do has an opposite effect.

2.2. The Light Curve of a Tidal Disruption Event

The light curves of candidate tidal disruption events (Komossa et al. 2004a) are characterized by rapid fall in X-ray luminosity on time scales of months to a year, followed by a gradual continued fading over the following decade. Three of the four candidate events (NGC 5905, RX J1420+53, RX J1242−11) are consistent with luminosity decay \(L_{\text{bh}} \propto t^{-5/3}\) expected if the X-ray emission is produced during the fallback of stellar debris onto a nascent accretion disk (Phinney 1989; Evans & Kochanek 1989). The fourth event RX J1624+75 exhibits what appears to be faster initial decay followed by very slow fading. In all cases, the total drop in X-ray luminosity is by a factor \(\sim 10^2-10^3\) over about a decade.

The above candidate tidal disruption events have been selected for characteristic, “outburst”-like light curves (fast rise and slow decay). However the true luminosity evolution of tidal disruption events is unknown. If the emission during the fallback stage is absorbed or otherwise suppressed, the X-ray light curve will be dominated by thin disk accretion and a quasi-steady flux over a longer period will be expected. Such events would remain undetected in existing searches that target outburst activity. To maintain generality, therefore, we consider fallback-like power-law light curves, and also discuss constant accretion rate models.

The power irradiated during fallback was derived in Li et al. (2002)

\[
L_{\text{bol}} \approx 4 \times 10^{32} \, \text{ergs s}^{-1} \left(\frac{f}{0.25}\right) \left(\frac{M_{\text{bh}}}{10^8 M_\odot}\right) \times \left(\frac{m_*}{M_\odot}\right)^{2/3} \left(\frac{t}{1 \, \text{yr}}\right)^{-5/3},
\]

where the tidal disruption occurs at \(t = 0\), and the luminosity reaches peak value and starts decaying as in equation (3) at time \(t_{\text{peak}} \approx 0.2 \left(M_{\text{bh}}/10^8 M_\odot\right)^{1/2} (m_* / M_\odot)^{11/3} (R_/R_\odot)^{3/2} \, \text{yr after tidal disruption.}

Although equation (3) was derived for the fallback process, we interpret it as a representative power-law decay model for the luminosity evolution, independent of the emission mechanism. To test the sensitivity to the power law index of luminosity decay, we consider decay of the form \(L_{\text{bol}} \propto t^{-\lambda}\) with \(\lambda > 1\) is a constant. We also test the sensitivity to the value of \(t_{\text{peak}}\) by scaling it via \(t_{\text{peak}}(\xi) = \xi t_{\text{peak}}(0)\). In both cases we keep
the total energy irradiated between \( t = t_{\text{peak}} \) and \( t = \infty \) constant and equal to \( f m_c c^2 \).

We also discuss an alternative to power-law light curves. Accurate theoretical modeling of a time-dependent thin disk emission is difficult. We therefore adopt a crude quasi-steady accretion scenario, in which we assume that accretion at constant rate proceeds “while the supplies last,” i.e., until all the bound debris has been accreted. This is inevitably an over-simplification. Taking into account the redistribution of mass in the disk [Cannizzo et al. 1990] estimate that under certain assumptions the light curve will be \( L_{\text{disk}} \propto t^{-1.2} \). On the other hand, if outer parts of the disk become thermally unstable and neutral, the accretion may be delayed [Menou & Quataert 2001].

In the “while the supplies last” constant-accretion scenario, we assume that the luminosity is a fraction \( \ell \) of the Eddington luminosity \( L_{\text{Edd}}(M_{\text{bh}}) \), and that the luminosity is related to the mass accretion rate via \( L = \ell c M_c^2 \), where as usual \( \ell \) parameterizes radiative efficiency. The duration of the active phase is then \( \Delta_{\text{active}} = \frac{c m_c^2}{L_{\text{Edd}}} \), implying a model luminosity \( L_{\text{bol}}(M_{\text{bh}}, t) = L_{\text{Edd}} \Delta_{\text{active}}(t) \), where \( H(x) \) is the Heaviside step function.

### 2.3. Integration over the Black Hole Mass Function

The LF of tidal disruption events is obtained by weighting the disruption probability modeled as a Poisson process by the black hole mass function. In the fallback model, the LF reads

\[
\Psi(L_X) = \int_{M_{\text{min}}}^{M_{\text{max}}} dM_{\text{bh}} \int_0^{\infty} dt \frac{\Psi(M_{\text{bh}})}{\Gamma(M_{\text{bh}})} e^{-\Gamma(M_{\text{bh}}) t} \times \delta(\omega - L_{\text{bol}}(M_{\text{bh}}, t) - L_X),
\]

where \( \omega \) is the bolometric correction, \( \delta(\cdot) \) is the Dirac \( \delta \)-function, and the dependence on \( f \) and \( m_c \) is implicitly assumed: for the radius of subsolar stars we adopt the relation \( R_* = R_{\odot}(m_*/M_{\odot})^{0.8} \) (e.g., [Kippenhahn & Weigert 1990]). Here, \( M_{\text{min}} \) is the minimum MBH mass, and as before \( M_{\text{max}} \propto m_c^{2/3} \) is the maximum MBH mass near which a star can be disrupted. We take \( M_{\text{min}} \sim 10^4 M_{\odot} \), as systems in which an even smaller black hole is expected have been found to lack one (e.g., [Merritt et al. 2001] [Valuri et al. 2005]). For the bolometric correction in the 0.5 – 2 keV band, we take \( \omega = 45 \), which at low luminosities is approximately independent of luminosity [Marconi et al. 2004] and references therein), although in reality the bolometric correction could be correlated with \( L_{\text{bol}}/L_{\text{Edd}} \) rather than \( L_{\text{bol}} \).

In Figure 1, we plot the resulting LF for our fiducial model with a light curve that decays as a power-law \( L \propto t^{-3} \) with \( \lambda = \frac{7}{5} \). The model is based on a galaxy LF with amplitude \( \Phi_0 = 0.02 \ h^{-3} \ Mpc^{-3} \) and absolute magnitude of an L, galaxy of \( M_B = -20.0 + 5 \log_{10} h \) [Blanton et al. 2001], where we assume \( h = 0.7 \). We vary the various parameters, including \( \lambda \) in Figure 1, to explore the sensitivity of the X-ray AGN LF to our choice of the fiducial model. In the low-luminosity regime \( L_X \ll L_{\text{peak}} \equiv \omega L_{\text{bol}}(m_c, t_{\text{peak}}(m_c)) \), the LF is a power-law \( \Phi(L_X) \propto L_X^{-\alpha} \). At \( L_X \gtrsim L_{\text{peak}} \sim 10^{44} (\omega/45)^{-1} m_c^{1/3} \text{ ergs s}^{-1} \), the LF drops precipitously.

Below \( L_X \sim 10^{44} \text{ ergs s}^{-1} \), the calculated X-ray AGN LF slightly overestimates but is roughly compatible with the soft X-ray AGN LF of [Haslanger et al. 2005] (shown in the figure), and is a factor of a few lower than the hard X-ray AGN LF [Ueda et al. 2003] [Barger et al. 2005]. The incompleteness of the soft X-ray LF resulting from obscuration.

In models with power-law decaying light curves, the low-luminosity slope of the AGN LF is determined by the power-law of the decay, rather than the shape of the black hole mass function (Figure 1H). The amplitude of the LF, however, is sensitive to the black hole mass function. The steep drop in the LF around \( 10^{44} \text{ ergs s}^{-1} \) is associated with the peak luminosity produced in a tidal disruption event, which corresponds to the peak mass inflow rate from the debris that is beginning to circularize around the black hole (Figure 1H).

In the “while the supplies last” model, where the accretion luminosity is a constant and equal to \( \ell L_{\text{Edd}} \), the LF reads

\[
\Psi(L_X) = \frac{\ell}{4 \pi G M_{\odot}} L_X \frac{m_c}{\Gamma(M_{\odot})} \Psi(M_{\odot}),
\]

for \( M_{\text{min}} < M_t < M_{\text{max}} \), where \( M_t = \omega \sigma T L_X / 4 \pi G M_{\odot} c \).

In the low luminosity regime, the LF is a power law \( \Psi(L_X) \propto L_X^{-\Delta/k} \), where \( \Delta/k < -1 \), although the two LFs have comparable amplitudes at \( L_X \sim 10^{43} \text{ ergs s}^{-1} \). The discrepancy may reflect a luminosity-dependent Eddington ratio \( \ell \). The dependence of \( \ell \) on luminosity or black hole mass is expected if the accretion rate is supply limited, rather than radiatively limited. For example, to reproduce \( \Psi(L_X) \propto L_X^2 \), we must have \( \ell \propto L_X \). At present it is not clear how such dependence should arise.

### 3. Discussion

While many theoretical uncertainties frustrate an accurate estimate of the contribution of activity associated with stellar tidal disruption to the X-ray LF of active galaxies, it seems that the contribution can be significant at low luminosities \( L_X \lesssim 10^{44} \text{ ergs s}^{-1} \). The tidal disruption activity makes a negligible contribution at higher luminosities (power-law profile of the measured soft X-ray LF extends to \( L_X \sim 10^{47.5} \text{ ergs s}^{-1} \) at redshifts \( z \sim 1 - 3 \)). MBHs with masses above \( \sim 10^7 M_{\odot} \) grow by accreting non-stellar material from the interstellar medium.

What is the origin of the featureless knee in the LF at \( L_X \sim (10^{31} - 10^{44}) \text{ ergs s}^{-1} \)? The location of the knee coincides with Eddington-limited accretion onto black holes with masses \( M_h \sim 10^7 M_{\odot} \). Given the tidal disruption rate assumed here (eq. 1), black holes with masses \( M_h \lesssim 2 \times 10^6 (f/0.25) M_{\odot} \), where \( f \) is the fraction of the stellar mass that ultimately gets accreted onto the MBH, could have grown to their present size by accreting stellar debris over a Hubble time, although undoubtedly, non-stellar accretion must have played a role. This critical mass is compatible with the location of the knee in the LF assuming near-Eddington accretion.

Black holes with masses \( \sim 10^7 M_{\odot} \), in turn, roughly lie at the demarcation line separating the dominance of late-type and early-type galaxies. If major mergers are responsible for diverting gas into accretion onto black holes in early type galaxies, then the absence of merging activity in late-type galaxies leaves stellar tidal disruption as a competitive supplier of material to the MBH. This may explain why the steep power-law behavior of the quasar LF fails to extend to lower luminosities.

The observed X-ray LF of AGN evolves with redshift. The number density of low-luminosity AGN increases by a factor

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1. The maximum accretion rate might exceed the Eddington limit by a factor of a few (e.g., [Begelman 2002]).
The frequency of hard X-ray outbursts in the AGN luminosity function will still be expected.

The relative contribution of stellar tidal disruptions to the X-ray AGN LF can be studied by examining long-term X-ray variability of the sources. Currently, long-term monitoring data have been analyzed for only a handful of sources (e.g., Markowitz & Edelson 2004). Theoretical uncertainty notwithstanding, the light curves of tidal disruption events should be characterized by a fast rise and slow decay, but the variability may or may not be detected as an outburst. The frequency of hard X-ray outbursts in the ROSAT All-Sky Survey was studied by Donley et al. (2002). Their estimate, $\sim 10^{-5}$ yr$^{-1}$ per galaxy, is significantly below the tidal disruption rate adopted by us. The rates can be reconciled if the majority of tidal disruptions do not exhibit outburst characteristics. In that case, a measurable asymmetry in the autocorrelation function will still be expected.

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The centers of galaxies with redshift, seems implausible.

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