Several types of extragalactic high-energy transients have been discovered, which include high-luminosity and low-luminosity long-duration gamma-ray bursts (GRBs), short-duration GRBs, supernova shock breakouts (SBOs), and tidal disruption events (TDEs) without or with an associated relativistic jet. In this paper, we apply a unified method to systematically study the redshift-dependent event rates and the global luminosity functions (GLFs; ignoring redshift evolution) of these transients. We introduce some empirical formulae for the redshift-dependent event rate densities for different types of transients and derive the local specific event rate density, which also represents its GLF. Long GRBs (LGRBs) have a large enough sample to reveal features in the GLF, which is best characterized as a triple power law (PL). All the other transients are consistent with having a single-power-law (SPL) LF. The total event rate density depends on the minimum luminosity, and we obtain the following values in units of $Gpc^{-3} yr^{-1}$: $0.8^{+0.7}_{-0.1}$ for high-luminosity LGRBs above $10^{50}$ erg s$^{-1}$; $164^{+28}_{-19}$ for low-luminosity LGRBs above $5 \times 10^{46}$ erg s$^{-1}$; $1.0^{+0.4}_{-0.0}$, $1.2^{+0.4}_{-0.3}$, and $3.3^{+0.8}_{-0.5}$ above $10^{50}$ erg s$^{-1}$ for short GRBs with three different merger delay models (Gaussian, lognormal, and PL); $1.9^{+2.4}_{-1.2} \times 10^4$ above $10^{44}$ erg s$^{-1}$ for SBOs, $4.8^{+3.2}_{-2.1} \times 10^2$ for normal TDEs above $10^{44}$ erg s$^{-1}$; and $0.03^{+0.04}_{-0.02}$ above $10^{48}$ erg s$^{-1}$ for TDE jets as discovered by Swift. Intriguingly, the GLFs of different kinds of transients, which cover over 12 orders of magnitude, are consistent with an SPL with an index of $-1.6$.

Key words: gamma-ray burst: general — stars: flare — stars: luminosity function, mass function — supernovae: individual (SN 2006aj)

1. INTRODUCTION

Extragalactic high-energy transients are intense cosmological transients whose electromagnetic emission peaks in the X-ray or $\gamma$-ray bands. The study of extragalactic high-energy transients has remained an active field in astrophysics over the years. Wide-field $\gamma$-ray detectors dedicated to study $\gamma$-ray bursts (GRBs) have led to discoveries of other types of high-energy transients, such as supernova shock breakouts (SBOs) and jets from tidal disruption events (TDEs). Upcoming wide-field X-ray telescopes (XRTs; e.g., Einstein Probe; Yuan et al. 2015) are expected to significantly enlarge the sample of the known high-energy transients and probably discover new types.

GRBs are the main extragalactic $\gamma$-ray transients. Their durations, usually described by $T_{\text{90}}$, range from milliseconds to thousands of seconds. Thanks to the extensive observations led by a list of $\gamma$-ray telescopes, such as BATSE, HETE-II, INTEGRAL, Swift, and Fermi, our understanding of GRBs has been greatly advanced. Two main types based on their durations are short GRBs (or SGRBs), with $T_{\text{90}} < 2$ s, and long GRBs (or LGRBs), with $T_{\text{90}} > 2$ s (Kouveliotou et al. 1993). Observations show that these two types of GRBs have distinct physical origins:4 massive star core collapses for LGRBs versus compact star mergers for SGRBs (see Kumar & Zhang 2015 for a recent review). Afterglow observations led to measurements of the redshifts of GRBs, allowing one to access the energetics of these events. Most LGRBs are found to have a typical isotropic luminosity ($1-10^4$ keV) in the range of $10^{51}-10^{53}$ erg s$^{-1}$, which are called high-luminosity long GRBs (HL-LGRBs). A small fraction of the observed LGRBs, on the other hand, have been detected with peak luminosities less than $10^{49}$ erg s$^{-1}$. Most of these events have distinct observational properties, such as long-duration, smooth, single-pulse light curves, and are usually referred to as low-luminosity long GRBs (LL-LGRBs). It has also been shown that LL-LGRBs have a much higher event rate density than HL-LGRBs (Soderberg et al. 2006). More importantly, they are found to form a distinct component in the GRB luminosity function (LF; Liang et al. 2007; Virgili et al. 2009), suggesting that they have a distinct physical origin. Recent studies (e.g., Campana et al. 2006; Wang et al. 2007; Waxman et al. 2007; Bromberg et al. 2011; Nakar & Sari 2012) suggested that at least some LL-LGRBs may be related to breakouts of trans-relativistic shocks from exploding massive stars.

Lacking a sensitive wide-field X-ray camera, the study of X-ray transients is only in its babyhood. Nonetheless, a few types of extragalactic X-ray transients have been discovered. TDEs, bright X-ray/UV flares generated when supermassive black holes (SMBHs) tidally disrupt stars, have been discovered from the archival X-ray survey data of the missions such as ROSAT, Chandra, and XMM-Newton (e.g., Bade et al. 1996; Komossa & Greiner 1999). These transients typically last for months to years, much longer than the duration of GRBs. The discovery of Sw J1644+57 (Burrows et al. 2011) by the Swift satellite suggested that some TDEs can have super-Eddington luminosities, which point toward a relativistic jet associated with the TDE event. The discovery of

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4 The duration classification sometimes leads to false identification of the physical category of GRBs; see Zhang et al. (2009) for a detailed discussion.
a thermal component associated with the prompt emission of the LL-LGRB 060218 led to the suggestion that the signal may be related to an SBO. A serendipitous discovery of an X-ray outburst (XRO) 080109 associated with a nearby supernova SN 2008D (Soderberg et al. 2008) suggested that there are indeed high-energy transients (even though with a much lower luminosity than LL-LGRBs) associated with SBOs. This discovery established SBOs as a new type of extragalactic high-energy transient.

There are several important questions regarding these transients: What are the event rate densities of them (i.e., how often do they occur per unit volume)? How do these event rate densities depend on redshift? What are the LFs of these transients? Do the LFs evolve with redshift? Addressing these questions is essential to understanding the progenitor systems of these transients and their cosmological evolution. A cross comparison among different transients may also shed light on possible common underlying physics behind these apparently different events.

In the literature, some studies have been carried out to address these questions for individual transients (e.g., Liang et al. 2007; Virgili et al. 2009; Wanderman & Piran 2010 for both HL-LGRBs and LL-LGRBs; Virgili et al. 2011b; Wanderman & Piran 2014 for SGRBs; Soderberg et al. 2008 for SBOs; Esquej et al. 2008 for normal TDEs; and Burrows et al. 2011 for jetted TDEs). Owing to the small sample size of some types of these transients, the estimates of their event rate densities are usually subject to large uncertainties. The total event rate density of a particular transient depends on the minimum luminosity and the shape of the LF, which is usually not well constrained. Also, the detectors’ sensitivity, search algorithms, and instrumental selection effects all introduce additional uncertainties to the problem. The calculations of the intrinsic event rate density rely on the sensitivity, field of view, and working period of the detectors. Since these transients have been detected using very different detectors with different sets of parameters, special care needs to be taken in order to obtain robust results.

In order to study the evolution of LFs, one needs a large enough sample that covers a wide redshift range, with each redshift bin having enough events to construct a statistically meaningful LF in the redshift bin. The X-ray transients we are studying mainly reside in the nearby universe, so that their meaningful LF in the redshift bin. The X-ray transients we are studying mainly reside in the nearby universe, so that their meaning full LF in the redshift bin having enough events to construct a statistically meaningful LF in the redshift bin. The X-ray transients we are studying mainly reside in the nearby universe, so that their meaningful LF in the redshift bin having enough events to construct a statistically meaningful LF in the redshift bin having enough events to construct a statistically meaningful LF in the redshift bin having enough events to construct a statistically meaningful LF in the redshift bin.

In this paper, we apply a unified method to systematically study the redshift-dependent event rate densities and the global LFs (GLFs; i.e., LFs derived ignoring possible redshift evolution) of several known extragalactic high-energy transients. For GRBs, thanks to their large sample size, we also investigate their LF evolution. Compared with previous studies, our analysis has a larger sample for most transients (especially for LL-LGRBs and TDEs), and more interestingly, we will derive the global event rate density distributions of all transients for the first time. In Section 2, we introduce the general methodology of calculating the event rate density and the LF of any type of transient. We then introduce redshift distributions of various transients in Section 3, especially the new empirical models for SGRBs and TDEs. In Section 4, we describe our data of all extragalactic high-energy transients. The results for individual events are presented in Sections 5.1 (LGRBs), 5.2 (SGRBs), 5.3 (SBOs), and 5.4 (TDEs), respectively. In Section 5.5, we present the global distribution of the LFs of all the transients. Conclusions are drawn in Section 6 with some discussion. Throughout the paper, the concordance cosmological parameters presented by the Planck Collaboration, i.e., $H_0 = 67.8$ km s$^{-1}$ Mpc$^{-1}$, $\Omega_m = 0.308$, $\Omega_\Lambda = 0.692$, are adopted (Planck Collaboration et al. 2015).

2. METHODOLOGY

2.1. Global Luminosity Function

Quantifying the redshift-dependent event rate density and LF of a certain type of transient is a challenging task. The observed events and their redshift and luminosity distributions are the results of the convolution of both (likely redshift-dependent) LF and intrinsic redshift distribution of the events, with the proper correction of the instrumental sensitivity threshold, field of view, and operational time. All these complications may be disentangled with a large enough observational sample. However, for most transients discussed in this paper (except GRBs), the number of observational samples is too small to perform such a task. In order to cross-compare various types of transients, in this paper we first ignore the possible redshift evolution of the LFs of all the transients and use the data to construct LFs of each type of transient. This allows us to separate LF and redshift distribution $f(z)$. In principle, the LF could be redshift dependent. For example, for LGRBs for which we have collected a large enough sample, evidence of such an evolution effect has been collected. As a result, the LF we construct in this paper only carries the meaning in the "global" sense. We hereby define all the LFs constructed without considering redshift evolution as GLFs. In order to use the data to construct the GLF, we also assume that the events with the same luminosity share the same other properties (e.g., spectral properties and detector parameters). This makes the observed events good indicators of the underlying general population. Also, since there is a wide range of the spectral peak energy ($E_{peak}$) distribution for different transients studied in this paper, we try as much as possible to apply the $k$-corrected bolometric luminosity ($10^{45}$eV) using the measured spectral properties of the transients (Equation (28)). The only exceptions are the TDEs detected by ROSAT, Chandra, and XMM-Newton, whose narrow bandpass does not allow a precise inference of the global spectral parameters. For these events, we use a uniform $k$-correction parameter 1.4 (Equation (30)).

For a certain type of transient, we define the local specific event rate density (local event rate density per unit luminosity)
The redshift-dependent event rate density can be written as

$$\rho_{0,L} = \frac{d\rho_0}{dL},$$

where $L$ denotes bolometric luminosity at the peak time hereafter. For a detector with flux sensitivity $F_{\text{th}}$, field of view $\Omega$, and operational time $T$, the detected number of events in the luminosity interval from $L$ to $(L + dL)$ is

$$dN = \frac{\Omega T}{4\pi} \rho_{0,L} dL \int_0^{\zeta_{\text{max}}(L)} \frac{f(z)}{1 + z} dV(z) dz$$

$$= \frac{\Omega T}{4\pi} \rho_{0,L} g(L) dL,$$

(2)

where

$$g(L) = \int_0^{\zeta_{\text{max}}(L)} \frac{f(z)}{1 + z} dV(z) dz.$$  

(3)

The dimensionless function $f(z)$ describes the redshift-dependent event rate density, i.e.,

$$\rho_L(z) = \rho_{0,L} f(z).$$

(4)

The redshift-dependent specific comoving volume reads (for the standard $\Lambda$CDM cosmology)

$$\frac{dV(z)}{dz} = \frac{c}{H_0 (1 + z)^2} \left[ \Omega_m (1 + z)^3 + \Omega_\Lambda \right]^{1/2}.$$  

(5)

For a particular $L$, the maximum redshift $\zeta_{\text{max}}(L)$, which defines the maximum volume inside which an event with luminosity $L$ can be detected, can be defined by the sensitivity threshold $F_{\text{th}}$ via

$$F_{\text{th}} = \frac{L}{4\pi D_L^2 (\zeta_{\text{max}}) k},$$

(6)

where $k$ is a correction factor, which corrects the observed flux in the detector’s energy band $(\epsilon_1, \epsilon_2)$ to a wide band in the rest frame (e.g., $1-10^4$ keV for GRBs; see Equation (29)).

Technically, it is easier to evaluate numbers in the logarithmic luminosity bins. Equation (2) can be also written as

$$dN = \frac{dN}{d\log L} d\log L = \frac{\Omega T}{4\pi} (\ln 10) \rho_{0,L} g(L) L d(\log L).$$

(7)

Suppose that $\Delta N$ events are detected in a finite logarithmic luminosity bin from log $L$ to log $(L + \Delta(\log L))$; one then has

$$\rho_{0,L} \approx \frac{4\pi}{\Omega T} \frac{1}{\ln 10} \frac{1}{g(L)} \frac{\Delta N}{L \Delta(\log L)}.$$  

(8)

The LF of a certain type of transient can be derived by displaying the specific event rate density $\rho_{0,L}(L) \propto \Phi(L)$ as a function of $L$. By separating the data into different luminosity bins, we use the observed numbers to map the relevant $\rho_{0,L}$ and then fit the data points by several empirical model forms. The simplest model is a single-power-law (SPL) form, i.e.,

$$\Phi(L) \propto L^{-\alpha}.$$  

(15)

If the model does not define the data well, we introduce a smoothly connected BPL form

$$\Phi(L) \propto \left[ \left( \frac{L}{L_0} \right)^{\alpha_0} + \left( \frac{L}{L_b} \right)^{\alpha_0} \right]^{-1/\omega},$$

(16)

where $\alpha_0$ and $\alpha_2$ are the PL indices before and after the break luminosity $L_b$, and $\omega$ defines the sharpness of the break. In more complicated cases (e.g., the GLF of LGRBs), one needs another PL segment to fit the data, and we introduce a triple-power-law (TPL) form, i.e.,

$$\Phi(L) \propto \left\{ \left[ \left( \frac{L}{L_{b,1}} \right)^{\alpha_0} + \left( \frac{L}{L_{b,2}} \right)^{\alpha_2} \right]^{-1/\omega} \left( \frac{L}{L_{b,1}} \right)^{-\alpha_1} \right\}^{-1/\omega_2} + \left\{ \left[ \left( \frac{L}{L_{b,2}} \right)^{\alpha_2} + \left( \frac{L}{L_{b,2}} \right)^{\alpha_0} \right]^{-1/\omega} \left( \frac{L}{L_{b,2}} \right)^{-\alpha_2} \right\}^{-1/\omega_2},$$

(17)
where $\alpha_1$, $\alpha_2$, and $\alpha_3$ are the PL indices for three segments, $L_{b,1}$ and $L_{b,2}$ are the two break luminosities, and $\omega_1$ and $\omega_2$ are the sharpness parameters at the two breaks.

### 2.2. LF Evolution of GRBs

GRBs have a large enough sample to study the redshift evolution effect. We investigate the evolution effect for LGRBs and SGRBs separately. For each class, we first separate the observed GRBs into several redshift bins and then apply our method to map the corresponding local specific event rate density using the GRBs in that specific redshift bin only.\(^5\) Practically, for a redshift bin $(z_1, z_2)$ around a certain redshift $z$, we change the integration limits in Equation (2) to $z_1$ and min $(z_2, z_{\text{max}}(L))$, respectively, and repeat the procedure laid out in Section 2.1. The derived local specific event rate density and event rate density are expressed as $\rho_{0,1}^c$ and $\rho_{0,2}^c$ respectively, denoting that they are derived in the redshift bin around $z$. Notice that $\rho_{0,1}^c$ still denotes the local value. By applying a proper correction with the redshift evolution function $f(z)$ (see details in Section 3), one can obtain the LF in the redshift bin $(z_1 < z < z_2)$. If GRB LF does not evolve with redshift, then the results derived from different $z$ bins should remain the same.

To minimize the truncation effect by the flux limits of the detectors, we also use a subsample with a higher threshold (with peak photon flux larger than 1.8 photons $s^{-1} \text{ cm}^{-2}$) in the derivations and compare the results with two thresholds.

Alternatively, we also repeat the analysis under the same assumption adopted in some recent papers (e.g., Pescalli et al. 2015; Petrosian et al. 2015; Yu et al. 2015), i.e., fix the shape of the LF and assume that $L_0$ evolves as a PL with $k \sim 2.3$. We can then map the LF from the data by correcting the luminosity $L$ at $z$ to the "local" value, i.e., $L_0 = L/(1+z)^{2.3}$. Applying the method in Section 2.1 using $L_0$ instead of $L$ would lead to the "local" LF.

### 2.3. Correction Factors

To perform our analysis, the redshift of an event is needed. For GRBs, not all events have redshift measurements. In order to properly account for their event rate density, one needs to correct the derived values based on the $z$-known sample by the ratio between the total number and the $z$-known event number.

\(^5\) There are some overlaps in adjacent redshift bins, since we want to include more GRBs in each bin to reach a better constraint of the corresponding LF.

### Table 1

**Instrumental Parameters**

| Detectors (Instrument) | Operation Time $(T)$ yrs | Field of View $(\Omega)$ sr | Sensitivity $(\text{erg cm}^{-2} \text{s}^{-1})$ $(F_{\text{th}})$ |
|------------------------|--------------------------|-----------------------------|---------------------|
| CGRO (BATSE)           | 10                       | $\pi$                       | $3.0 \times 10^{-8}$ |
| HETE-II (NXM)          | 7                        | 0.8                         | $8.0 \times 10^{-9}$ |
| INTEGRAL (IBIS)        | 12                       | 0.26                        | $9.1 \times 10^{-9}$ |
| Swift (XRT)            | 10                       | $5 \times 10^{-5}$         | $10^{-12}$          |
| ROSAT (PSPC)           | 8                        | $10^{-3}$                   | $3.0 \times 10^{-13}$ |
| XMM-Newton (EPIC)      | 15                       | $2 \times 10^{-4}$         | $2.0 \times 10^{-14}$ |
| Chandra (ACIS)         | 14                       | $6 \times 10^{-4}$         | $4.0 \times 10^{-15}$ |
| Swift (BAT)            | 10                       | 1.33                        | $3 \times 10^{-8}$ for HL-LGRBs and rate-triggered LL-GRBs |
| Swift (BAT)            | 10                       | 1.33                        | $10^{-7}$ for SGRBs  |
| Swift (BAT)            | 10                       | 1.33                        | $2.8 \times 10^{-9}$ for LL-LGRB 060218/100316D |
| Swift (BAT)            | 10                       | 1.33                        | $10^{-8}$ for Sw J1644+57 |
| Swift (BAT)            | 10                       | 1.33                        | $4.3 \times 10^{-11}$ for Sw J2058+05 |

For HL-LGRBs and SGRBs, this correction factor is approximately 3, and we adopt it in our derivations.

The detected rates also depend on the detector’s spectral window. For GRBs, BATSE observations suggested that the short-to-long ratio is about 1:3 (Paciesas et al. 1999), whereas Swift BAT, which has a softer bandpass, only gets a 1:10 ratio (Sakamoto et al. 2011; Qin et al. 2013). Since Swift can essentially detect all BATSE LGRBs, one needs to correct for the Swift-detected SGRBs by another factor of $\sim 3$ for the inferred SGRB event rate density. This factor has been taken into account in our derivations.

For the other types of transients, the samples are not large enough to access whether we have missed some events owing to the imperfect instrumental spectral window or the lack of redshift measurements. We therefore derive the event rate density using the observed events only.

### 2.4. Instrumental Parameters

The three important instrumental parameters that are relevant to our derivations are the operation time $(T)$, the field of view $(\Omega)$, and the flux sensitivity threshold $(F_{\text{th}})$. Table 1 lists the three parameters of the high-energy detectors used to study various high-energy transients discussed in this paper. While the first two parameters are straightforwardly defined, the definitions of sensitivity thresholds are nontrivial. This is particularly true for wide-field triggering detectors such as Swift BAT, with which most of the GRBs and jetted TDEs were detected (e.g., Lien et al. 2014 for a detailed description of the Swift BAT trigger algorithm). In this paper, we adopt an approximate threshold for each detector. For Swift-detected events, we also adopt slightly different values for different types of events.

Most GRBs were detected through the rate trigger algorithm by BAT, whereas some low-flux events, such as the LL-LGRB 060218, were detected through an image trigger algorithm. The image trigger is an additional trigger algorithm to accumulate photons from a source in a comparably longer time to look for transients that are not bright enough to make a rate trigger.

For the rate-trigger GRB events detected by Swift/BAT, we adopt slightly different values for different subtypes. In order to have the redshift of a GRB measured, the burst usually needs to have a bright enough optical afterglow. On average, the $z$-known GRBs are brighter and therefore have a higher flux threshold than the standard rate trigger flux threshold. Based on
the lowest value of the flux distributions of our subsample, we adopt $F_{\text{th}} = 3 \times 10^{-8} \text{erg cm}^{-2} \text{s}^{-1}$ for rate-triggered LGRBs (including HL-LGRBs and LL-LGRB 080517) and $10^{-7} \text{erg cm}^{-2} \text{s}^{-1}$ for SGRBs.

Taking HL-LGRBs as an example, we derive the flux threshold based on the lower end of the observed photon flux distribution. We adopt the photon flux $0.3 \text{ photons cm}^{-2} \text{s}^{-1}$ as the threshold. The transformation from photon flux to specific flux (Equation (26)) requires the information of the spectrum. We consider a typical Band function spectrum (Band et al. 1993) with $\alpha = -1$, $\beta = -2.3$, $E_{\text{peak}} = 200 \text{ keV}$ at redshift $z = 1$. This threshold photon flux is translated to $F_{\text{th}} = 3 \times 10^{-8} \text{erg cm}^{-2} \text{s}^{-1}$.

The LL-LGRBs 060218 and 100316D and the two Swift-detected TDE jets were detected through image trigger. In the case of image trigger algorithm, the threshold function depends on the trigger duration $T_{\text{th}}$ with the dependence $F_{\text{th}} \propto T_{\text{th}}^{-1/2}$. The trigger duration of GRB 060218 was about $80 \text{s}$, with a mean flux of $\sim 2.8 \times 10^{-9} \text{erg cm}^{-2} \text{s}^{-1}$ (T. Sakamoto 2015, private communication). This roughly corresponds to a threshold flux

$$F_{\text{th}} = 2.5 \times 10^{-8} T_{\text{th}}^{-1/2} \text{erg cm}^{-2} \text{s}^{-1},$$

which we adopt to also calculate the threshold flux for other image trigger events. The trigger duration of GRB 100316D is $64 \text{s}$. The two jetted TDE events Sw J1644+57 and Sw J2058+05 had a trigger duration of $64 \text{s}$ (Burrows et al. 2011) and 4 days (Cenko et al. 2012), respectively, and the corresponding $F_{\text{th}}$ are used to derive $\rho_{\text{OL}}$ of jetted TDEs. In fact, Sw J1644+57 was image-triggered four times. The $64 \text{s}$ trigger duration was the relevant one at the peak luminosity.

XRO 080109 was serendipitously discovered by Swift XRT. We use a count rate of 0.03 counts s$^{-1}$ for XRT, with which source variability can be detected for a $\sim 1000 \text{s}$ observation. This corresponds to a flux threshold $F_{\text{th}} \sim 10^{-12} \text{erg cm}^{-2} \text{s}^{-1}$.

Normal X-ray TDEs were usually discovered from archival survey data of various X-ray missions, such as the ROSAT PSPC All-Sky Survey (RASS; Voges et al. 1999), the XMM-Newton Slew Survey Source Catalog (XMMSSlc; Saxton et al. 2008), and the Chandra ACIS archival data. The exposure-time-dependent flux sensitivity thresholds of these three detectors are listed in Table 1. For each TDE event, we consider the real exposure time to determine its $F_{\text{th}}$.

3. REDSHIFT DISTRIBUTION

The redshift distribution parameter $f(z)$ for each type of transient is essential to infer the local (specific) event rate density (Section 2), and different types of transients may have different $f(z)$ functions. In this section, we discuss this function for different types of transients in detail.

3.1. LGRBs and Supernova SBOs

LGRBs (both HL and LL) and SBOs are associated with the deaths of massive stars. To first order, their redshift distribution should track the history of star formation. There is evidence that at high $z$, the GRB rate may exceed what the star formation history (SFH) predicts (e.g., Kistler et al. 2008; Li 2008; Qin et al. 2010; Virgili et al. 2011a; Robertson & Ellis 2012). However, for a wide redshift span, the SFH is a good proxy of the redshift distribution of LGRBs. In this paper, we adopt the rough analytical model of SFH derived by Yüksel et al. (2008) using the observational data:

$$f_{\text{GRB/SBO}}(z) = \left[ (1 + z)^{2.4\eta} + \frac{1 + z}{5000} \right]^{-0.3\eta} + \left( \frac{1 + z}{9} \right)^{-3.5\eta},$$

where $\eta = -10$. At $z < 4$, this function is directly derived from the SFH inferred from the UV and far-IR galaxy data (Hopkins & Beacom 2006), which is independent of the GRB observations. At $z = 5−7$, the SFH is enhanced from the galaxy-constrained SFH to compensate the observed GRB excess at high $z$, which can be explained by the deficiency of the observed low-luminosity star-forming galaxies missed in surveys but traced by GRBs. We adopt Equation (19) to study both LGRBs and SBOs. The latter are only observed in the nearby universe, so that the modification at high $z$ does not enter the problem.

3.2. Short GRBs

Unlike LGRBs, most SGRBs do not directly trace SFH. Observations suggest that most SGRBs are consistent with having an origin not related to massive star deaths. The leading scenario is mergers of double compact star systems, e.g., two neutron stars (NS–NS) or a neutron star and a black hole (NS–BH; Gehrels et al. 2004; Barthelmy et al. 2005; Fox et al. 2005; Fong et al. 2010; see Berger 2014 for a recent review).

In order for a merger to occur, a compact star binary system needs to go through a long inspiral phase defined by energy loss of the system through gravitational wave radiation. The redshift distribution of SGRBs therefore needs to account for an additional time delay due to inspiral with respect to the creation of the compact binary system, which itself traces the SFH. The distribution of the merger delay timescale is unfortunately not known. Practically, one assumes some empirical forms of the merger delay timescale distribution models and applies the data to derive best parameters for the delay model. Three types of merger delay time models have been discussed in the literature (e.g., Virgili et al. 2011b; Wanderman & Piran 2014 and references therein): PL delay model, Gaussian delay model, and lognormal delay model. Current data support either a Gaussian (Virgili et al. 2011b) or lognormal (Wanderman & Piran 2014) delay model, with the (PL) model disfavored (even though not completely ruled out; Virgili et al. 2011b; Wanderman & Piran 2014). Table 2 lists the three models with the best parameters currently constrained by the SGRB data.

With the consideration of the merger delay time distribution, it is difficult to construct an analytical model for the redshift distribution of SGRBs. Instead, we perform a series of Monte Carlo simulations based on the SFH and merger...
Table 2
Best-fit Merger Delay Models of SGRBs with Respect to Star Formation History

| Delay Model       | Formula                                      | Best-fit Parameters | Reference       |
|-------------------|----------------------------------------------|---------------------|-----------------|
| Gaussian (G)      | $m_G(\tau)d\tau = \exp\left(-\frac{(\tau - \frac{3.5G}{2})^2}{2\sigma_G^2}\right)\frac{1}{\sqrt{2\pi}\sigma_G}d\tau$ | $t_G = 2$ Gyr, $\sigma_G = 0.3$ | (1)             |
| Lognormal (LN)    | $m_{LN}(\tau)d\ln \tau = \exp\left(-\frac{\ln(\tau) - \ln(\sigma_{LN})}{\sigma_{LN}}\right)\left(\frac{\tau}{\sqrt{2\pi}\sigma_{LN}}\right)d\ln \tau$ | $t_{LN} = 2.9$ Gyr, $\sigma_{LN} = 0.2$ | (2)             |
| Power law (PL)    | $g_{PL}(\tau)d\tau = \tau^{-\alpha}d\tau$ | $\alpha = 0.81$ | (2)             |

References. (1) Virgili et al. 2011b; (2) Wanderman & Piran 2014.

![Figure 1](image_url)  
Figure 1. Redshift distribution derived from Monte Carlo simulations for short GRBs considering three delay time models with respect to star formation history: Gaussian (black), lognormal (blue), and PL (red). For each model, the result is derived from the average of 10,000 simulations, each with simulated 10,000 systems. Dots are the simulated results, and the curve is the empirical multiple-PL fit given in Equations (20)–(22).

delay distribution models to construct several redshift distributions that correspond to the three delay models with the best-fit parameters. First, we randomly generate 10,000 compact star binary systems with a redshift distribution tracking the SFH following the model of Yüksel et al. (2008). Next, we randomly generate the merger delay timescales of all these systems based on the three merger delay timescale models listed in Table 2. For each model, we derive the lookback time of SGRBs by subtracting the merger delay time from the formation time, and we transfer the lookback time to redshift. We repeat the process 10,000 times (each with 10,000 events simulated). By averaging the results, we are able to derive the average redshift distribution of the simulated samples. We fit the derived redshift distribution (for all three merger delay models) using multiple-PL functions and derive an empirical expression of $f(z)$ for each model. The simulated results with best-fit empirical models are shown in Figure 1. The distributions are normalized to unity at the local universe ($z = 0$). The empirical formulae of $f(z)$ for the three merger delay models are as follows.

For the Gaussian delay model (Virgili et al. 2011b), one has

$$f_{SGRB}^G(z) = \left[\left(1 + z\right)^{5.0\eta} + \left(\frac{1 + z}{0.17}\right)^{0.87\eta}\right] + \left(\frac{1 + z}{4.12}\right)^{-8.0\eta} + \left(\frac{1 + z}{4.05}\right)^{-20.5\eta}.$$

(20)

with $\eta = -2$, which is roughly a BPL with redshift breaks at $z_1 = 0.45$, $z_2 = 2.0$, and $z_3 = 3.0$.

For the lognormal delay model (Wanderman & Piran 2014), one has

$$f_{SGRB}^{LN}(z) = \left[\left(1 + z\right)^{5.7\eta} + \left(\frac{1 + z}{0.36}\right)^{1.3\eta}\right] + \left(\frac{1 + z}{3.3}\right)^{-9.5\eta} + \left(\frac{1 + z}{3.3}\right)^{-24.5\eta}.$$

(21)

with $\eta = -2$, which is roughly a BPL with redshift breaks at $z_1 = 0.35$, $z_2 = 1.5$, and $z_3 = 2.3$.

For the PL model (Wanderman & Piran 2014), one has

$$f_{SGRB}^{PL}(z) = \left[\left(1 + z\right)^{3.9\eta} + \left(\frac{1 + z}{2.5}\right)^{1.2\eta}\right] + \left(\frac{1 + z}{3.8}\right)^{-4.4\eta} + \left(\frac{1 + z}{7.7}\right)^{-11.0\eta}.$$

(22)

with $\eta = -2.6$. This model has a wider redshift distribution compared to the first two models (owing to the wide range of the merger delay time). It is roughly a BPL with redshift breaks at $z_1 = 0.42$, $z_2 = 3.4$, and $z_3 = 11.3$. The SGRB data do not
favor this model (Virgili et al. 2011b), even though it is not completely ruled out.

3.3. Tidal Disruption Events

The event rate density of TDEs depends on both the number density of SMBHs and the event rate of TDEs per galaxy. Since the TDE rate of a particular SMBH only depends on the properties of the galaxy itself (e.g., stellar density near the SMBH and the mass of SMBH), on average, it may be reasonable to assume that there is no redshift evolution of the event rate per galaxy. As a result, the $f_{\text{TDE}}(z)$ parameter of TDEs is mostly determined by the evolution of the number density of SMBHs as a function of redshift (e.g., Donnarumma & Rossi 2015). Shankar et al. (2013) constructed the mass density distribution models for SMBHs and active galactic nuclei (AGNs) by considering their growth rate and radiation efficiency. We apply their model to derive $f_{\text{TDE}}(z)$ for TDEs. TDEs can happen only when the tidal disruption radius is larger than the event horizon of SMBHs, which gives an upper limit of the mass of SMBHs for TDEs:

$$M_{\text{BH}} \lesssim 1.6 \times 10^9 \left( \frac{M_*}{M_\odot} \right) \left( \frac{R_*}{R_\odot} \right)^{3/2}, \quad (23)$$

where $M_*$ and $R_*$ are the mass and radius of the star that is disrupted by the SMBH, both normalized to the solar values. We therefore exclude SMBHs with mass exceeding $10^9 M_\odot$.

In the left panel of Figure 2, we present the numerical fit to the number density redshift evolution of SMBHs with two mass ranges ($10^5 - 10^7 M_\odot$ and $10^7 - 10^8 M_\odot$). Assuming a constant TDE rate per galaxy, in the right panel of Figure 2, we present the normalized TDE redshift distribution $f_{\text{TDE}}(z)$ derived from the numerical data based on the model of Shankar et al. (2013). The best-fit empirical model reads

$$f_{\text{TDE}}(z) = \left[ \left( 1 + z \right)^{0.2\eta} + \left( \frac{1 + z}{1.43} \right)^{-3.2\eta} + \left( \frac{1 + z}{2.66} \right)^{-7.0\eta} \right]^2, \quad (24)$$

with $\eta = -2$. One can see that $f_{\text{TDE}}(z)$ continues to decrease with redshift, reaching $2/5$ at $z \sim 1$ and $\sim 10^{-3}$ at $z \sim 6$.

4. DATA

4.1. Gamma-ray Bursts

Our HL-GRB sample is only limited to Swift GRBs. This is because it is a uniform sample whose size is large enough to derive a well-constrained GLF. We collect all the $z$-known Swift GRBs before 2014 May 6 (250 HL-LGRBs and 20 SGRBs). This sample consists of more GRBs than previous work by introducing a lower flux threshold, which allow us to better study the features near the low-luminosity end. The data are downloaded from the Swift archival table available at http://swift.gsfc.nasa.gov/archive/grb_table/ (Sakamoto et al. 2008, 2011). For all the bursts, the 1 s peak photon flux and photon index are recorded. For HL-LGRBs, the 1 s peak photon flux is directly derived from their 1 s peak luminosity. For SGRBs, since their durations are typically shorter than 1 s, we apply a photon count rate with a 64 ms resolution to derive the 64 ms peak luminosity. We calculate their 64 ms peak photon flux based on the ratio of the two peak count rates with different temporal resolutions ($C_{\text{p},64\text{ ms}}$ and $C_{\text{p},1\text{ s}}$), i.e., $P_{64} = P_1\left(C_{\text{p},64\text{ ms}}/C_{\text{p},1\text{ s}}\right)$. The 64 ms light curves are from the Swift Burst Ground-analysis Information page (http://gcn.gsfc.nasa.gov/swift_gnd_ana.html), and the 1 s light curves are obtained through rebinning. To ensure the correct match at the peak, the regrouping is such that the time interval at the peak time (64 ms resolution) matches the one for the 1 s peak photon flux provided in the GCN Circular archive. Only a handful of LL-LGRBs were detected so far. Table 3 collects the information of six LL-LGRBs studied in this paper, which were...
triggered not only by \textit{Swift} (GRB 060218, GRB 080517, and GRB 100316D) but also by other instruments as well: GRB 980425 by \textit{CGRO}/\textit{BATSE}, XRF 020903 by \textit{HETE-II} \footnote{The acronym “XRF” stands for “X-ray flashes.” They are softer versions of GRBs. Observations show that XRFs and GRBs seem to form a continuum in the observational and theoretical parameter spaces (Sakamoto et al. 2004; Zhang et al. 2004; Bersier et al. 2006). In fact, GRB 060218 can be also called an XRF. We adopt the names of these events based on the convention adopted in their discovery papers.} and GRB 031203 by \textit{INTEGRAL}. The peak photon fluxes of pre-
\textit{Swift} LL-LGRBs are adopted from GCN archives or Sakamoto et al. (2004). The data of \textit{Swift} LL-LGRBs are also taken from the
\textit{Swift} table.

The time-integrated spectral information is taken from the literature (references provided in Table 3), described by either an SPL with photon index $\Gamma(N(E) \propto E^{-\Gamma})$, a Band function characterized by peak energy $E_{\text{peak}}$ and two photon spectral indices $\alpha$ and $\beta$ (Band et al. 1993), or a PL function with an exponential cutoff (CPL) fit, i.e., $N(E) \propto E^\alpha \exp\left(-E/E_0\right)$. For the latter two models, an $E_{\text{peak}}$ can be derived from the peak in the $\nu F_{\nu}$ spectrum. For SPL fits to most BAT spectra (owing to the narrowness of the BAT band), it is believed that the intrinsic spectrum still has a peak energy. With BAT GRBs jointly detected by other wide-band detectors such as \textit{Konus}/Wind and \textit{Fermi}/GBM, it was found that there exists a rough correlation between the BAT-band photon index $\Gamma$ and $E_{\text{peak}}$ if $E_{\text{peak}}$ is not much beyond the BAT energy band (Zhang et al. 2007; Sakamoto et al. 2009; Virgili et al. 2012). The latest best fit reads (Virgili et al. 2012)

$$\log(E_{\text{peak}}) = (4.34 \pm 0.475) - (1.32 \pm 0.129) \Gamma_{\text{BAT}}$$

with a large scatter, where $\Gamma_{\text{BAT}}$ is photon index (positive value) defined in the BAT band. We apply this scaling to estimate $E_{\text{peak}}$ for those GRBs whose $E_{\text{peak}}$ is not directly measured. For a consistency check, we have also adopted $E_{\text{peak}}$ values derived by Butler et al. (2007) for a subsample of GRBs (for which $E_{\text{peak}}$ is available from that method). By repeating the calculations, we found that the derived LF using the Butler et al. (2007) method is similar to the LF derived using our method.

For a GRB with peak photon flux $P_p$, the peak flux can be calculated through

$$F_p = \frac{P_p \int_{E_1}^{E_2} EN(E)dE}{\int_{E_1}^{E_2} N(E)dE},$$

where $N(E)$ is the photon spectrum of a GRB, which is in the form of the standard Band function (Band et al. 1993)

$$N(E) = \begin{cases} \left(\frac{E}{100 \text{ keV}}\right)^\alpha \exp\left(-\frac{E}{E_0}\right), & E < (\alpha - \beta)E_0, \\ \left[(\alpha - \beta)E_0\right]^\beta \exp(\beta - \alpha)\left(\frac{E}{100 \text{ keV}}\right)^\beta, & E \geq (\alpha - \beta)E_0. \end{cases}$$

Here the integration limits $(e_1, e_2)$ enclose the detector’s energy window (e.g., 15–150 keV for \textit{Swift} BAT). For SGRBs, we use the $E_{\text{peak}}$ data of 13 SGRBs derived by Lü et al. (2015). For the other seven SGRBs whose $E_{\text{peak}}$ was not directly measured, we estimate $E_{\text{peak}}$ using Equation (25). For those GRBs whose Band function parameters are not directly measured, we adopt typical values as $\alpha = -1$ and $\beta = -2.3$ for LGRBs and $\alpha = -0.5$ and $\beta = -2.3$ for SGRBs.

In order to derive the bolometric luminosity (1–10$^4$ keV in the cosmological rest frame) from the observed peak flux, we perform a $k$-correction

$$L_{p, \text{bol}} = 4\pi D_L^2 F_p \cdot k,$$

where $D_L$ is the luminosity distance. The $k$-correction parameter can be expressed as

$$k = \frac{\int_{E_1}^{10^4/(1+z)} EN(E)dE}{\int_{E_1}^{E_2} EN(E)dE}.$$
4.2. Shock Breakouts

Massive stars end their lives in catastrophic core collapses when they run out of fuel in the center (Woosley & Weaver 1986). As a massive star undergoes core collapse, an outgoing shock surges through the star. When the optical depth of photons trapped in the shock becomes unity, a SBO occurs, which provides the first electromagnetic emission from a supernova event. Before the shock breaks out of the star, only ultraviolet or X-rays depending on how compact the star is. As the shock surges through the star, the optical depth of photons becomes unity, a SBO occurs, which provides the first electromagnetic emission from a supernova event. Before the shock breaks out of the star, only ultraviolet or X-rays depending on how compact the star is.

\[ L_{\text{bol,46}} = \frac{L_{\text{bol}}}{10^{46}} \]

The bolometric luminosity of XRO 080109 is calculated from k-correction based on a power-law spectrum with photon index of 2.3. \[ L_{\text{bol,46}} \] is in units of \(10^{46}\) erg s\(^{-1}\).

4.3. Tidal Disruption Events

Stellar tidal disruption by an SMBH has been theoretically predicted by Rees (1988). When a star approaches an SMBH, a TDE occurs if the tidal force becomes larger than the self-gravity of the star and if the radius when this happens is outside the black hole event horizon. Part of the disrupted debris falls into the black hole from an accretion disk, giving rise to a bright flare in UV or X-ray band, which lasts from several months to 1 yr. The first TDE was discovered in quiescent galaxy NGC 5905 during the RASS (Bade et al. 1996; Komossa & Bade 1999), which showed the characteristic luminosity decay law \( L \propto t^{-5/3} \) expected for fallback accretion. Later, several more TDEs were detected from RASS, namely, RX J1242, RX J1624, and RX J1420 (Grupe et al. 1999; Komossa & Greiner 1999; Greiner et al. 2000). In the recent decade, more TDE candidates have been discovered by XMM-Newton and Chandra, mostly by comparing catalogues with archival data (Esquej et al. 2007, 2008; Maksym et al. 2010; Saxton et al. 2012; Maksym et al. 2013), as well as by serendipitous detections (Lin et al. 2011). Another ROSAT source was identified as a TDE candidate as it disappeared in the subsequent observations with XMM-Newton and Chandra (Cappelluti et al. 2009). Right now about a dozen X-ray TDE candidates have been discovered. All these TDEs have large amplitudes and soft X-ray spectra, whose host galaxies show no sign of AGN activity (Komossa 2012).

Table 4

| Name                  | Detector | Energy Band | \( L_{\text{bol,46}} \) | Redshift | Reference       |
|-----------------------|----------|-------------|-------------------------|----------|-----------------|
| SN 2006aj/GRB 060218  | Swift (BAT) | 15–150 keV | 14.7                    | 0.033    | Campana et al. (2006) |
| SN 2008D/XRO 080109   | Swift (XRT) | 2–10 keV    | 0.0061                  | 0.007    | Soderberg et al. (2008) |

Note.

\(^a\) The bolometric luminosity of XRO 080109 is calculated from k-correction based on a power-law spectrum with photon index of 2.3. \( L_{\text{bol,46}} \) is in units of \(10^{46}\) erg s\(^{-1}\).
both the rising and the declining phases, so that the peak luminosity cannot be well constrained. The maximum luminosity during the detected phase is only the lower limit of the peak luminosity. However, since the light-curve peak is rounded and spreads in several weeks (Lodato et al. 2009), the observed peak luminosity may not be too different from the true peak luminosity.

Owing to the narrow bandpass of the XRTs that detect TDEs, the spectral shape for TDEs is not well constrained. Except for the BAT-detected TDEs for which a treatment similar to GRBs can be applied, for the majority of TDEs, we only apply an empirical relation to estimate the bolometric luminosity by multiplying X-ray luminosity by a factor of 1.4, i.e. (Maksym et al. 2010),

\[ L_{p,\text{bol}} = 1.4 \times L_p. \]  

(30)

For Swift TDEs, a PL spectrum in the BAT band is reported for both events with a photon index of 1.8 and 1.6, respectively (Burrows et al. 2011; Cenko et al. 2012). Even though the spectrum of jetted TDEs is not known, we speculate that they have a nonthermal spectrum with \( L_{p,\text{bol}} \approx 10^{38} \) erg s\(^{-1}\). In the second approach, we derive the LF of LGRBs jointly by fitting the data together with a two-component (i.e., TPL) LF. This approach is justified in view of the fact that both LL-LGRBs and HL-LGRBs are associated with SNe Ic and therefore may share a common physical origin.

5.1.1. Global LF

Figure 3 shows the results of GRBs. The event rate density above a particular \( L \) as a function of the bolometric luminosity \( L \) is presented in the left panel, and the specific event rate density as a function of \( L \), which describes the GLF, is presented in the right panel. In both panels, the HL-LGRBs (red), LL-LGRBs (blue), and SGRBs (black) are presented separately. The luminosity bin is taken as 0.3 (LGRBs) or 0.7 (SGRBs) in the logarithmic space. The horizontal errors denote the luminosity bins, whereas the vertical errors are calculated from small-sample statistics (Gehrels 1986). The best-fit lines for all three subtypes of GRBs are also presented. The fitting results are summarized in Tables 6 and 7. For all the fitting parameters, we also present the 1\( \sigma \) range of errors based on 5000 sets of Monte Carlo simulations.

The local event rate density of LL-LGRBs is \( 16^{+7}_{-5} \times 10^{-3} \) Gpc\(^{-3} \) yr\(^{-1} \) with a minimum luminosity \( 5 \times 10^{46} \) erg s\(^{-1} \), which is roughly consistent with previous results (Liang et al. 2007; Virgili et al. 2009). The longer working period of Swift until now than the ones relevant for the previous two papers makes the event rate density slightly lower than before. However, it is still around two orders of magnitude higher than that of HL-LGRBs, which is \( 2.4^{+0.3}_{-0.2} \) Gpc\(^{-3} \) yr\(^{-1} \) above \( 3 \times 10^{49} \) erg s\(^{-1} \), or \( 0.8^{+0.1}_{-0.0} \) Gpc\(^{-3} \) yr\(^{-1} \) above \( 10^{50} \) erg s\(^{-1} \) (a typical luminosity threshold adopted before). This local event rate of HL-LGRBs is slightly lower than Liang et al. (2007) and Wanderman & Piran (2010).

From Equation (13), one can see that \( \rho_{\Lambda} \) is proportional to the LF \( \Phi(L) \), with \( \rho_0 \) defining the normalization. We use either an SPL or a TPL to fit the \( \rho_{\Lambda} \) distribution for each subtype of GRBs to characterize their GLFs. The fitting results are shown in Table 6. HL-LGRBs can be fit with a TPL with \( \alpha_{\text{HL}} = 2.2^{+0.4}_{-0.2} \), \( \beta_{\text{HL}} = 1.0^{+0.1}_{-0.0} \), \( \alpha_{\text{HL}} = 2.0^{+0.3}_{-0.3} \), and the break luminosity \( L_{\text{HL}}^{\text{break}} = 5.0^{+3.0}_{-1.3} \times 10^{50} \) erg s\(^{-1} \). The luminosity distribution of LL-LGRBs can only be fit using an SPL with \( \alpha_{\text{LL}} = 2.3^{+0.2}_{-0.2} \). The LL-LGRBs are not the

### Table 5

| Name       | Detector | Energy Band | \( L_{p,\text{bol}}^a \) | Redshift | Reference                  |
|------------|----------|-------------|--------------------------|----------|----------------------------|
| NGC 5905   | ROSAT    | 0.1–2.4 keV | \( 3.6 \times 10^{33} \) | 0.011    | Bade et al. (1996); Komossa & Bade (1999) |
| RX J1242   | ROSAT    | 0.1–2.4 keV | \( 1.2 \times 10^{34} \) | 0.05     | Komossa & Greiner (1999)    |
| RX J1624   | ROSAT    | 0.1–2.4 keV | \( 2.2 \times 10^{34} \) | 0.064    | Grupe et al. (1999)        |
| RX J1420   | ROSAT    | 0.1–2.4 keV | \( 7.6 \times 10^{34} \) | 0.147    | Greiner et al. (2000)      |
| NGC 3599   | XMM      | 0.2–2.0 keV | \( 7.1 \times 10^{34} \) | 0.0028   | Esquej et al. (2007); Esquej et al. (2008) |
| SDSS J1324 | XMM      | 0.2–2.0 keV | \( 6.7 \times 10^{34} \) | 0.088    | Esquej et al. (2007); Esquej et al. (2008) |
| TDXF J1347 | ROSAT    | 0.3–2.4 keV | \( 8.8 \times 10^{32} \) | 0.037    | Cappelluti et al. (2009)   |
| SDSS J1311 | Chandra  | 0.3–3.0 keV | \( 7.0 \times 10^{32} \) | 0.195    | Maksym et al. (2010)       |
| 2XMMA J1847| XMM      | 0.2–2.0 keV | \( 3.9 \times 10^{31} \) | 0.035    | Lin et al. (2011)          |
| SDSS J2011 | XMM      | 0.2–2.0 keV | \( 4.2 \times 10^{31} \) | 0.146    | Saxton et al. (2012)       |
| WINGS J1348| Chandra  | 0.2–2.0 keV | \( 2.8 \times 10^{32} \) | 0.062    | Maksym et al. (2013)       |
| Swift J1644+57 | Swift | 15–150 keV | \( 7.2 \times 10^{38} \) | 0.354    | Bloom et al. (2011); Burrows et al. (2011) |
| Swift J2058+05 | Swift | 15–150 keV | \( 7.6 \times 10^{37} \) | 1.185    | Cenko et al. (2012)        |

**Note.**

\(^a L_{p,\text{bol}} \) is in units of erg s\(^{-1} \).
straightforward extension of HL-LGRBs to low luminosities. But the slope of LL-LGRB is similar to that of the first component of HL-LGRBs. The normalization of LL-LGRBs is a little bit lower as we apply a lower threshold for LL-LGRBs than HL-LGRBs. Therefore, it may be possible that LL-LGRBs follow the extension of LF of HL-LGRBs if we take a TPL fit to the joint LL and HL samples. Such a fit is presented in Figure 4, with the best-fit parameters being \( \alpha_1 = 1.7^{+0.1}_{-0.1}, \alpha_2 = 1.0^{+0.2}_{-0.1}, \alpha_3 = 2.0^{+0.3}_{-0.3} \) and the break luminosities \( L_{b,1} = 1.0^{+0.2}_{-0.3} \times 10^{51} \text{ erg s}^{-1}, L_{b,2} = 7.8^{+2.3}_{-3.1} \times 10^{52} \text{ erg s}^{-1} \). This is similar to the TPL fit to HL-LGRBs alone except for a slightly shallower \( \alpha_1 \), which is compromised by the slight mismatch between LL-LGRBs and HL-LGRBs.
The TPL nature of the joint GLF for LGRBs is interesting. Such a feature was only noticeable in the past when LL-LGRBs are included (Liang et al. 2007; Virgili et al. 2009). With the current sample, we find that it is required even for HL-LGRBs alone. With the joint fit LL- and HL-LGRBs, we find that the steep component in the low-luminosity end now extends all the way to \( \sim 10^{53} \) erg s\(^{-1} \), so that no clear separation between the LL- and HL-LGRB population is seen.

We would like to stress that if we focus on the two high-\( L \) segments in the GLF, our results (\( \alpha_2 \sim 1.0, \alpha_3 \sim 2.0, L_{b,2} \sim 7.8 \times 10^{52} \) erg s\(^{-1} \)) are broadly consistent with previous results: \( \alpha_{\text{HL}} \sim 1.0, \beta_{\text{HL}} \sim 2.6, \) and \( L_{b,\text{HL}} \sim 2.5 \times 10^{52} \) by Liang et al. (2007), and \( \alpha_{\text{HL}} \sim 1.17, \beta_{\text{HL}} \sim 2.44, \) and \( L_{b,\text{HL}} \sim 3.1 \times 10^{52} \) erg s\(^{-1} \) by Wanderman & Piran (2010).\(^{11} \)

According to Equations (1) and (11), the indices of \( \rho_{0,>L} \) and \( \rho_{0,L} \) should be roughly the same, i.e., the index of \( \rho_{0,L} \) should be greater than the index of \( \rho_{0,>L} \) by one. This is generally satisfied for most of the transients studied in this paper (see all the indices marked in Figures 3–8).

### 5.1.2. Luminosity Function Evolution

Using the method laid out in Section 2.2, we study the evolution effect of LGRB LF. The results of \( \rho_{0,L} \) are shown in the left panel of Figure 5. For each redshift bin, we fit the LF with an SPL or BPL if the latter is needed. The fitting parameters are presented in Table 8. One can see that indeed there is an apparent LF evolution effect. However, there is no clear pattern to quantify the evolution. The right panel of Figure 5 shows the redshift-dependent break luminosity. In some redshift bins a break is clearly seen. However, in some other bins, the break either does not exist or is simply required by only one data point with low significance. For SPL fits, we place either a lower limit or an upper limit based on the highest- or lowest-luminosity bin. As shown in the right panel of Figure 5, there is no clear pattern to quantify the evolution effect. Furthermore, the PL indices \( \alpha_1 \) and \( \alpha_2 \) also show significant evolutions (variations) in different redshift bins.

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11 Notice that \( \alpha_{\text{HL}} \) and \( \beta_{\text{HL}} \) in previous works correspond to \( \alpha_2 \) and \( \alpha_3 \) in our notation. Also, Wanderman & Piran (2010) derived the LF in the logarithmic space, so the \( \alpha \) and \( \beta \) values in their notation are smaller by one from our values.

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Since different redshift bins have different \( L_m \), and since the behavior below \( L_m \) is poorly constrained by the data, in Table 8 we choose different \( L_m \) for different redshift bins. For the nearby universe, we also get a \( \rho_{0,L} \) at higher \( L_m \). We obtain a consistency of \( \rho_{0,L} \) derived from data from different redshift intervals.

To minimize the truncation effect by the flux limit of detectors, we also use a subsample with a higher threshold (with peak photon flux larger than 1.8 photons s\(^{-1} \) cm\(^{-2} \)); see Figure 6. The subsample consists of fewer GRBs in some redshift intervals (e.g., \( z \in (0.5, 1.5) \)) so that the LF can be fit by an SPL. In the nearby universe, on the other hand, since LL-LGRBs are dropped owing to this high-threshold criterion, the LF demands a TPL fit.\(^{12} \) The fitting parameters are also presented in Table 8. The evolution of \( L_0 \) is now better quantified by \( L_0 \sim (1+z)^{3.7} \) (Figure 6, right panel), but a significant variation of \( \alpha_1 \) and \( \alpha_2 \) values in different redshift bins remains. We therefore conclude that there is no straightforward way to quantify the evolution effect of the LGRB LF.

On the other hand, if we assume the evolution law assumed from the latest papers (e.g., Pescalli et al. 2015; Petrostian et al. 2015; Yu et al. 2015), i.e., the PL indices remain unchanged, and only \( L_0 \) evolves with \( k \sim 2.3 \), we can map the LF from the data by correcting the luminosity \( L \) at \( z \) to the “local” value, i.e., \( L_0 = L/(1+z)^{2.3} \) to derive the “local” LF. The result is shown in Figure 7. This local LF can be fit by a BPL with \( \alpha_1 \sim 1.5, \alpha_2 \sim 2.5, \) and \( L_{b,0} \sim 51.6 \) erg s\(^{-1} \). This is consistent with the results presented in previous papers.

### 5.2. SGRBs

#### 5.2.1. Global LF

The local event rate density for SGRBs varies slightly for different merger delay models. For a minimum luminosity \( 7 \times 10^{50} \) erg s\(^{-1} \), it is \( 4.2^{+1.3}_{-1.0} \times 3.9^{+1.2}_{-0.5} \times 7.1^{+2.3}_{-1.7} \) Gpc\(^{-3} \) yr\(^{-1} \) for the Gaussian, lognormal, and PL delay models, respectively. Taking a typical minimum luminosity \( 10^{50} \) erg s\(^{-1} \) as adopted by previous authors, the numbers are \( 1.3^{+0.4}_{-0.3} \times 1.2^{+0.4}_{-0.3} \times 3.3^{+0.9}_{-0.8} \) Gpc\(^{-3} \) yr\(^{-1} \), respectively. The local event rate density for the lognormal model is slightly lower than the value reported by Wanderman & Piran (2014), as we use a slightly lower flux threshold for Swift BAT-detected SGRBs.

SGRBs come with a much smaller number of events than LGRBs. Assuming that all the SGRBs with redshift measurements are of a compact star merger origin, we derive their LF in Figure 8. The three different merger delay models give slightly different results, but in general all three models are consistent with having an SPL LF with an index of \( \sim 1.6 \) (for details, see Figure 6). This is different from HL-LGRBs, which require a TPL LF. It is also different from Wanderman & Piran (2014), who claimed a BPL LF.

One caveat of our treatment is the assumption that all SGRBs are of a compact star merger (Type I) origin. In the Swift era, Zhang et al. (2009) first suspected that some high-\( L \) SGRBs at high redshifts may not be of the Type I origin, but may rather originate from massive star core collapse (Type II). They suggested to apply multiwavelength criteria (instead of using \( \gamma \)-ray duration only) to judge the physical origin of a
GRB. Later Virgili et al. (2011b) pointed out that the assumption that all SGRBs are of the compact star merger origin (Type I) is disfavored since one cannot simultaneously account for the $z - L$ two-dimensional distribution and the $N - \log \, P$ distribution of SGRBs. They claimed that a good fraction of SGRBs may be of a Type II origin. Bromberg et al. (2013) recently reached the similar conclusion using a different argument based on the duration distribution of GRBs. Wanderman & Piran (2014) used the criteria of Bromberg et al. (2013) and excluded about 1/3 of SGRBs that they suspect to be of a massive star core collapse origin. This may explain the difference between the results of this paper (SPL LF) and that paper (BPL). We did not exclude any SGRB from our sample for the following reason. We believe that any conclusion about the physical category of an SGRB based on the duration information only (e.g., Bromberg et al. 2013) is not reliable. Rather, one should consider multiwavelength criteria (Zhang et al. 2009), especially the host galaxy type and the afterglow location within the host. Host galaxy studies of SGRBs (Fong et al. 2010; Berger 2014) suggested that the hypothesis that all SGRBs belong to the compact star merger (Type I) category is not in conflict with the data. Indeed, some SGRBs excluded by Wanderman & Piran (2014; defined by them as collapsars) actually have large offsets from host galaxies, fully consistent with being due to a compact star merger origin (e.g., GRB 070724 with offset 5.46 \pm 0.14 kpc, and GRB 070809 with offset 33.22 \pm 2.71 kpc; Fong et al. 2010; Fong & Berger 2013). Furthermore, a recent study of SGRB emission amplitude parameter (Lü et al. 2014) also suggested that most observed SGRBs are not disguised SGRBs due to the “tip-of-iceberg” effect. Even though we believe that there exists a contamination of Type II GRBs in the SGRB sample, without studying the multiwavelength data of SGRBs in

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**Figure 5.** Left panel: LF of long GRBs in different redshift bins for the full sample. Blue dots denote the LL-LGRBs. Magenta, red, green, cyan, and black dots represent HL-LGRBs from $0 < z < 1$, $0.5 < z < 1.5$, $1 < z < 3$, $2 < z < 4$, and $z > 3$, respectively. Best-fit models are overplotted as solid curves with the corresponding color. Right panel: break luminosity evolution inferred from the LF fit from the left panel. The medium values of each redshift bin are taken. For dubious BPL, we give both an upper limit (the minimum luminosity of data; lower triangle) and a lower limit (derived from BPL fit; upper triangle). No clear evolution pattern is observed.

**Figure 6.** Same as Figure 5, but for a subsample with peak photon flux larger than 1.8 photons s$^{-1}$ cm$^{-2}$. In the redshift bin $0.5$–$1.5$ (red), the sample is fit by an SPL. The lower/upper limits of the break luminosity (red triangles in the right panel) are derived from the maximum and minimum luminosities of the data. These limits are not used in the $L_b$ fit (the dashed line in the right panel).

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1.9 the SGRB sample into three redshift bins study the possible evolution effect of LF. We manage to divide bins. The results are shown in Figure 9. The LFs can be all any SGRB in this study. (LFs for SGRBs with three different merger delay models: Gaussian Figure 8. For SGRBs that have much less data, it is more difficult to be drawn. The event rate densities at different luminosity bins have a wide distribution, ranging from over $10^3$ Gpc$^{-3}$ yr$^{-1}$ at $10^{42}$ erg s$^{-1}$ to $\sim 10^2$ Gpc$^{-3}$ yr$^{-1}$ at $10^{45}$ erg s$^{-1}$. In the luminosity range of $(10^{33}-10^{44})$ erg s$^{-1}$, the event rate density is in the range of $(10^3-10^5)$ Gpc$^{-3}$ yr$^{-1}$, which is consistent with both theoretical predictions (Wang & Merritt 2004) and the estimates based on observations (Esquej et al. 2008; Luo et al. 2008; Maksym et al. 2010). The event rate density of the two Swift TDEs is $\sim 0.03_{-0.02}^{+0.04}$ Gpc$^{-3}$ yr$^{-1}$. Similar to GRB 060218, these two events were detected through image triggers. In particular, Sw J1644+57 triggered BAT multiple times (all image triggers; Burrows et al. 2011). We use the brightest peak to define the peak luminosity, and we derive the event rate density based on the trigger information of that epoch. The GLF of TDEs is roughly described by an SPL with $\alpha_{\text{TDE}} = 2.0$. With the current sample, the jetted TDEs detected by Swift seem to lie in the extension of a normal TDE LF to high luminosities. The event rate density of Sw J1644+57 shows a flattening feature at the highest luminosity. More data are needed to verify whether jetted TDEs form a distinct component in the global TDE LF.

### 5.5. Global Distribution

In Figure 12, we plot all high-energy transients in one figure. The left panel shows the local event rate density above a certain luminosity ($\rho_{0, L}$) as a function of $L$, and the right panel presents the specific local event rate density ($\rho_{0, L}$), which essentially represents the GLF. All the data points are given a $1\sigma$ error in vertical axis. The width of the luminosity bin is shown as the horizontal error bar.

Intriguingly, all the transients seem to line up to form a rough SPL distribution. A best fit to the GLFs of all the transients gives a slope of $\alpha_{\text{global}} = 1.6$. All the events lie within the $3\sigma$ confidence bounds of the best fit. The region below this correlation line is likely due to an observational bias and could be filled with new types of transients. With a
much lower event rate density, these transients may not have been detected within the time span of the modern high-energy astronomy. The region above the correlation line, on the other hand, is not subject to selection effects and must be intrinsic. The existence of such an upper boundary of high-energy transients is intriguing, which may be rooted from more profound physical reasons.

6. CONCLUSIONS AND DISCUSSION

In this paper, we systematically investigated the local event rate density, redshift evolution, and GLF of several known extragalactic high-energy (γ-ray and X-ray) transients, including HL-LGRBs and LL-LGRBs that have a massive-star core-collapse origin, SGRBs that likely have a compact star merger origin, supernova SBOs, and TDEs of stars by SMBHs. Our conclusions can be summarized as follows.

1. For all types of transients, the GLFs are typically well described by an SPL, although that of HL-LGRBs demands a TPL.

2. The local event rate density of each type of transient depends on the minimum luminosity. For GRBs, we get \( \rho_{0,L_{\text{m}}} = 164^{+66}_{-50} \text{Gpc}^{-3} \text{yr}^{-1} \) with \( L_{\text{m}} = 5 \times 10^{50} \text{erg s}^{-1} \) for LL-LGRBs, \( \rho_{0,L_{\text{m}}} = 2.4^{+0.3}_{-0.3} \text{Gpc}^{-3} \text{yr}^{-1} \) with \( L_{\text{m}} = 3 \times 10^{49} \text{erg s}^{-1} \) for HL-LGRBs, and \( \rho_{0,L_{\text{m}}} = 4.2^{+1.3}_{-1.0} \text{Gpc}^{-3} \text{yr}^{-1} \) for SGRBs, with \( L_{\text{m}} = 7 \times 10^{49} \text{erg s}^{-1} \) for the Gaussian, lognormal, and PL merger delay models, respectively. Even with two confirmed cases, the SBOs have event rate densities that cover a wide range, from \( 3.1^{+4.0}_{-2.1} \times 10^{44} \text{erg s}^{-1} \) for XRO 080109/SN 2008D-like events (luminosity \( \sim 6.1 \times 10^{43} \text{erg s}^{-1} \)) to \( 11^{+25}_{-10} \text{Gpc}^{-3} \text{yr}^{-1} \) for GRB 060218/ SN 2006aj-like events (luminosity \( \sim 1.5 \times 10^{47} \text{erg s}^{-1} \)). The event rate density of SBOs also covers a wide range, from \( 1.0^{+0.4}_{-0.3} \times 10^{5} \text{Gpc}^{-3} \text{yr}^{-1} \) with \( L_{\text{m}} = 10^{52} \text{erg s}^{-1} \) for normal SBOs to \( 0.03^{+0.04}_{-0.02} \text{Gpc}^{-3} \text{yr}^{-1} \) above 10^{48} \text{erg s}^{-1} \) for jetted SBOs detected by Swift.

3. For GRBs, we confirmed the previous work (Liang et al. 2007; Virgili et al. 2009) that LL-LGRBs still do not straightforwardly follow the extension from HL-LGRBs. However, a TPL fit to the entire LGRB population suggests that the steeper GLF slope in the low-energy end now extends to a much higher luminosity, so that LL- and HL-LGRBs are no longer clearly separated. Consider that the GLF shape in the high-L end, the indices (\( \alpha = 1.0, \beta = 2.0 \)), and the break luminosity (\( L_{\text{b}} = 7.8 \times 10^{52} \text{erg s}^{-1} \)) are generally consistent with (even though not identical to) what was found in previous work (Liang et al. 2007; Wanderman & Piran 2010). For SGRBs, we found a SPL LF with \( \alpha_{\text{GRB}} = 1.6 \), in contrast with the BPL distribution found by Wanderman & Piran (2014). The discrepancy may lie in different sample selection...
whereas Wanderman & Piran (2014) excluded about 1/3 of SGRBs, we included all the SGRBs in our analysis.

4. We confirm the conclusion of previous authors (e.g., Pescalli et al. 2015; Petrovian et al. 2015; Yu et al. 2015) that the LF of LGRBs likely evolves with redshift. However, we find that the evolution cannot be easily quantified with a simple analytical model. Nonetheless, if one assumes that the shape of the LF does not change and only the break luminosity evolves with redshift, results consistent with those of previous authors can be achieved.

5. SBOs and LL-LGRBs have a similar index $\alpha_{\text{SBO}} = \alpha_{\text{LL-LGRB}} = 2.0$, supporting the idea that LL-LGRBs may be related to SBOs (Campana et al. 2006; Wang et al. 2007; Waxman et al. 2007; Bromberg et al. 2011; Nakar & Sari 2012).

6. The GLF of TDEs is consistent with an SPL with $\alpha_{\text{TDE}} = 2.0$. The jetted TDEs discovered by Swift seem to be consistent with the extension of normal TDEs to the high-luminosity regime, even though a flattening feature is seen. More data are needed to judge whether jetted TDEs form a new component in the GLF.

7. Intriguingly, all the high-energy transients are consistent with having a global SPL distribution of GLFs with a slope of 1.6. Even though there could exist transients below the line that have not been discovered, the lack of events above the line is real. The existence of such an upper boundary is intriguing, and its physical origin is unknown.

8. To perform this analysis, we adopted/derived the redshift distribution factor $f(z)$ of various types of transients based on different models. For LGRBs and SBOs, we assume that the event rate density traces the SFH and adopt the empirical model (Equation (19)) of Yüksel et al. (2008). For SGRBs, through Monte Carlo simulations, we derived empirical $f(z)$ functions for three merger delay models: Equations (20)–(22) for the Gaussian, lognormal, and PL, respectively. For TDEs, we assume that the event...
rate is constant within each galaxy, and we derived an empirical formula of $f(z)$ (Equation (24)) based on the black hole number density evolution following Shankar et al. (2013). These empirical formulae can be directly used in the future.

This paper focuses on high-energy transients only, serving as a reference for the wide-field γ-ray astronomy and the upcoming wide-field X-ray astronomy (led by, e.g., Einstein Probe; Yuan et al. 2015). We notice that the phenomenology of all the transients studied in this paper extends to lower frequencies in the electromagnetic spectrum. For example, GRBs have multiband wavelength afterglows. SBOs can peak in the UV or even optical band if the progenitor star is large enough. UV and optical TDEs and radio counterparts of jetted TDEs have been discovered. The study of high-energy transients in the low-frequency domain is beyond the scope of this paper.

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Figure 12. Global distributions of all extragalactic high-energy transients. Left panel: event rate density above a minimum luminosity with respect to bolometric luminosity; right panel: joint LF. Different types of events are marked in different colors. An SPL fit (red line) and 3σ boundary for the correlation are presented.
