Mottness underpins the anomalous optical response of Iron Pnictides

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(Dated: October 9, 2008)

The recent discovery of high-temperature superconductivity (HTSC) in doped Iron pnictides is the latest example of unanticipated behavior exhibited by d- and f-band materials. The symmetry of the SC gap, along with the mechanism of its emergence from the “normal” state is a central issue in this context. Here, motivated by a host of experimental signatures suggesting strong correlations in the Fe-pnictides, we undertake a detailed study of their normal state. Focussing on symmetry-unbroken phases, we use the correlated band structure method, LDA+DMFT, to study the one-particle responses of both LaO1−xFexAs and SnO1−xFexAs in detail. Building on excellent quantitative agreement between LDA+DMFT and key experiments probing the one-particle responses, we extend our study, undertaking the first detailed study of their normal state electrodynamic response. In particular, we propose that near-total normal state incoherence, resulting from strong, local correlations in the Fe d-shell in Fe-pnictides, underpins the incoherent normal state transport found in these materials, and discuss the specific electronic mechanisms leading to such behavior. We also discuss the implications of our work for the multi-band nature of the SC by studying the pairing “glue” function, which we find to be an overdamped, electronic continuum. Similarities and differences of cuprates and Fe-pnictides are also touched upon. Our study supports the view that SC in Fe-pnictides arises from a bad metallic, incoherent “normal” state that is proximate to a Mott insulator.

PACS numbers: 74.25.Jb, 72.10.-d, 74.70.-b

I. INTRODUCTION

Discovery of high-,$T_c$ superconductivity (HTSC) in the Fe-based pnictides\textsuperscript{1} is the latest among a host of other, ill-understood phenomena characteristic of doped d- and f-band compounds. HTSC in Fe-pnictides emerges upon doping a bad metal with spin density wave (SDW) order at q = (π, 0). Preliminary experiments indicate\textsuperscript{2,3} unconventional SC. Extant normal state data indicate a “bad metal” with anomalously high resistivity (Ω·cm) even at low temperature.\textsuperscript{4} These observations in Fe-pnictides are reminiscent of underdoped cuprate SC. The small carrier density, along with Uemura scaling from μ-SR\textsuperscript{5} similar to hole-doped cuprates strongly suggests a SC closer to the Bose condensed, rather than a BCS limit. A brief general review\textsuperscript{6} gives a chemist’s overview on the subject.

Several theoretical works have addressed the issue of the “degree of correlated electronic” behavior in Fe-pnictides.\textsuperscript{7,8} This is an important issue, bearing as it does upon a characterization of charge and spin fluctuations: are they itinerant\textsuperscript{9,10} or closer to localized?\textsuperscript{11} This itinerant-localized \textit{duality} is a recurring theme in correlated systems in general\textsuperscript{12} and in fact is at the root of early formulations of the Hubbard model itself.\textsuperscript{13}

In Fe-pnictides, HTSC results from the Fe d band states hybridized with As p states: this leads to two hole, and two electron-like pockets in one-electron bandstructure calculations. Within weak coupling HF-RPA studies of effective, two- and four-orbital Hubbard models\textsuperscript{9,14} this gives a q = (π, 0) SDW order, in seeming agreement with inelastic neutron scattering (INS) results.\textsuperscript{15} Observation of quasi-linear (in T) behavior in the resistivity, pseudogap in optical reflectance\textsuperscript{16} and a spin gap in NMR\textsuperscript{17} in doped Fe-pnictides, among other observations, however, are benchmark features showing the relevance of strong, dynamical spin and charge correlations in the pnictides. In analogy with cuprates, this suggests that the Fe-pnictides might be closer to a Mott insulator (MI) than generally thought.\textsuperscript{2} Actually, the undoped pnictides of the A1−xFexAs type with A = La, Sr, the so-called “111” pnictides, show an insulator-like resistivity \textit{without} magnetic order for $T^* > 137$ K\textsuperscript{18} dependent upon the specific Fe-pnictide considered. Onset of bad metallic behavior correlates with a structural (tetragonal-orthorhombic (T-O)) distortion at $T^*$, \textit{below} which SDW order sets in. This is different from the AFe$_2$As$_2$ pnictides with A = Ba, Sr (the so-called “122” pnictides), where the bad metallic resistivity is observed only above $T^*$. Nevertheless, as we will discuss below, optical measurements on the 122 family also indicate a non-Fermi Liquid (nFL) metallic behavior at low T. So due care must be exercised when one attempts to classify Fe-pnictides into the “weakly” or “strongly” correlated category. The small carrier number seemingly generated upon the structural distortion in the 111 pnictides accords with the observed high resistivity, lending further credence to such a view.

Optical conductivity is a time-tested probe for characterizing the charge dynamics in solids. Specifically, it measures how a particle-hole pair excitation, created by an external photon field, propagates in the system, uncovering the detailed nature of the excitation spectrum itself. In a normal Fermi liquid (FL), low-energy scattering
processes leave the identity of an excited electron (hole) intact. This fact, noticed first by Landau, implies a long lifetime for excited quasiparticles: near the Fermi surface, their lifetime, \( \tau^{-1}(\omega, T) \approx \omega^2, T^2 \), greatly exceeds \( \omega, T \), their energy. In optical response, this fact manifests itself as the low-energy Drude part (after subtracting the phonon contribution), corresponding to coherent propagation of particle-hole excitations built from such quasiparticles. The Drude parametrization, a lorentzian with half-width \( \Gamma = \tau^{-1}(\omega, T) \)

\[
\sigma(\omega) = \frac{ne^2}{m^*} \frac{1}{1 + i\omega\tau(\omega)}
\]  
(1)
describes the low-energy optical response of normal metals. This allows one to estimate the transport relaxation rate and dynamical mass from

\[
\frac{1}{\tau(\omega)} = \frac{N e^2}{m_0} Re \left[ \frac{1}{\sigma(\omega)} \right]
\]
(2)

and

\[
m^*(\omega) = \frac{N e^2}{\omega} Im \left[ \frac{1}{\sigma(\omega)} \right].
\]
(3)

With \( \sigma(\omega) \approx \Gamma/(\omega^2 + \Gamma^2) \) at low-energy, \( m^*(\omega) = m_0 \), a constant. As long as the FL survives, even in \( f \)-band rare-earth metals with \( e-e \) interactions much larger than the (band) kinetic energy, this observation holds. Observation of a non-Drude optical conductivity in clean metals with low residual resistivity is thus a diagnostic for non-FL charge dynamics, i.e., where \( \tau^{-1}(\omega) \approx \omega^2, m^* = const \) at low energy no longer hold. One can, however, continue to use the Drude parametrization, at the cost of having a complicated \( \omega \)-dependence of \( \tau^{-1}, m^* \) at low energy. Such non-FL optical conductivity in the symmetry-unbroken bad-metallic phases is characteristic of several strongly correlated systems, from quasi-one dimensional Luttinger liquids\(^{19}\) high-\( T_c \) cuprates up to optimal doping\(^{20}\) \( f \)-electron systems close to quantum phase transitions\(^{20}\) and MnSi\(^{21}\) among others. Additionally, strongly correlated \( d \)- and \( f \)-band FL metals routinely exhibit a non-Drude optical response above a low-\( T \) scale, the so-called lattice coherence scale (\( O(1-20) \) K), below which correlated FL behavior obtains.\(^{17}\) So the material diversity and range of distinct ground states exhibited by the above strongly suggests a common underlying origin of the anomalous charge dynamics. The known importance of strong, short-ranged electronic correlations in \( d \)-and \( f \)-band systems then implies that Mott-Hubbard physics may underlie such generic, anomalous features.

On the theoretical side, observation of non-Drude, incoherent, or power law optical response forces one to discard the Landau FL theory, together with perturbation theory in interactions upon which it is based: an electron (hole) is no longer an elementary excitation of the system. The one-fermion propagator exhibits a branch cut analytic structure, leading to power-law fall-off in optics. This reflects the fact that the action of the electronic current operator (within linear response theory)\(^{22}\) does not create well-defined elementary excitations at low energy, leading to an incoherent response.

II. EARLIER WORK

Extant LDA+DMFT (local-density approximation plus dynamical mean-field theory) works on Fe-pnictides give either a strongly renormalized FL\(^{23}\) or an orbital selective (OS), incoherent, pseudogapped metal.\(^{24}\) Very good semiquantitative agreement with key features seen in both photoemission (PES) and X-ray absorption (XAS) for SmO\(_{1-x}\)Fe\(_x\)As\(^{23,24}\) as well as with the low-energy (15 meV) kink in PES is obtained using LDA+DMFT.\(^{25}\) Focusing on the “normal” state of Fe-pnictides, is LDA+DMFT adequate for describing their correlated electronic structure, or are cluster extensions (cluster-DMFT) of DMFT needed? If the observed SDW order has its origin in a Mott-Hubbard, as opposed to a weak-coupling Slater-like SDW picture, one would expect that incorporation of “Mottness”\(^{26}\) is adequate, at least in the symmetry unbroken phases (\( T > T^* \) at \( x = 0 \) and at all \( T > T_c \), the SC transition temperature, for doped cases) without SDW/SC order. If two-particle spectra, e.g., the optical conductivity, could be described within the same picture, this would serve as strong evidence for relevance of large \( D \) (DMFT) approaches in this regime. Specifically, given that vertex corrections in the Bethe-Salpeter equations for the conductivity identically vanish in \( D = \infty \)\(^{27}\), a proper description of the optical response of SmO\(_{1-x}\)Fe\(_x\)As within DMFT would imply negligible vertex corrections, justifying use of DMFT \textit{a posteriori}.

An optical study on La- and Sm-oxypnictides has already been carried out.\(^{28,29}\) While detailed spectral weight analysis remains to be done, characteristic strong correlation features are already visible: a small “Drude” peak, weak mid-infra red feature, and a slowly decreasing contribution up to high energy, \( O(2.0) \) eV in La-pnictides, and a power-law like decay of the reflectance in Sm-pnictide, all testify to this fact, and accord with their bad metallic resistivity. Onset of SC in SmO\(_{1-x}\)Fe\(_x\)As\(_x\) results in reflectivity changes over a broad energy range\(^{28}\) a characteristic signature of underlying “Mottness”. Apart from these common features, there are quantitative differences in results from different groups.\(^{28,29}\) These can be traced back to the fact that while an effective medium approximation is invoked for SmO\(_{1-x}\)Fe\(_x\)As\(_x\),\(^{29}\) no such analysis is performed for LaO\(_{1-x}\)FeAs\(_x\).\(^{28}\) Given the intrinsic polycrystalline nature of the samples used by both, as well as the differences in analysis, this may not be surprising. Optical work on single-crystal samples is thus highly desirable; this may be close at hand. Nevertheless, with these caveats, these observations are strongly reminiscent of cuprates up to optimal doping.\(^{31}\) and constrain theories to un-
understand SC as an instability of an incoherent, non-FL metallic state. More recently, Yang et al. have indeed performed a detailed analysis of optics for single crystals of Ba$_{0.53}$K$_{0.47}$Fe$_2$As$_2$. Slow (in energy, \( \omega \)) decay in reflectivity and an anomalously large \( \tau^{-1}(\omega) \) with sub-linear \( \omega \) dependence, implying no FL quasiparticles, reinforce similar features found in earlier optical results for La- and Sm-oxypnictides. Further, an extraction of the \( \alpha^2 F(\omega) \) bosonic “glue” reveals strong coupling to the low-energy bosonic fluctuation modes (due to inter-orbital, coupled charge-spin density modes?). Observation of non-FL quasiparticle features in optics implies that these bosonic modes are themselves strongly overdamped. Strong inelastic scattering from short-ranged, dynamical spin, charge and orbital correlations can indeed lead to such behavior, as has been investigated more extensively in the cuprate context. More studies are required to check whether these features are generic for Fe-pnictides: in view of incoherent features already seen in all investigated cases, we believe that this will indeed turn out to be the case.

In what follows, we compute the correlated band structure and optical conductivity of both La- and SmO$_{1-x}$Fe$_x$As$_y$, extending previous work, where very good semiquantitative agreement with the one-particle spectrum was found. We show how “Mottness” in the Fe \( d \)-bands underpins the charge dynamics in Fe-pnictides. In particular, we show how an excellent theory versus experiment comparison for the one-particle spectral function (DOS) is obtained for doped La$_{0.12}$Fe$_{0.88}$AsF$_x$, and build upon this agreement to obtain very good quantitative agreement with the reflectivity as well. Armed with this agreement, we analyze these theoretical results in detail and predict specific non-FL features that should be visible in future experimental work. Finally, we estimate the “glue function”, \( \alpha^2 F(\omega) \), and propose that it should be understood as an electronic (multiparticle) continuum that can be interpreted as an overdamped bosonic spectrum. We conclude with a brief qualitative discussion of its implications for SC.

### III. CORRELATED BAND STRUCTURE

The bare one-electron band structure of both LaOF$_x$As and SmOFeAs used in this work was computed using the linear muffin-tin orbital (LMTO) scheme in the atomic sphere approximation (ASA). As evidenced in several studies, the overall structures are remarkably similar in both cases, confirming that the active electronic states involve the carriers in the FeAs layers. Shown in Fig. 1, the orbital-induced anisotropies in the band structure are manifest: the \( xy \), \( 3z^2-r^2 \) bands are almost gapped at the Fermi energy \( E_F \), while the \( xx, yz, x^2-y^2 \) bands have appreciable weight at \( E_F \). The only essential difference between the LDA DOS for La- and Sm-pnictides is that in the latter case, due to larger chemical pressure (caused by the smaller size of Sm relative to La), the LDA band width is slightly \( (O(0.5 \text{ eV})) \) larger. The one-electron part of the Hamiltonian for Fe-pnictides is then given by,

\[
H_0 = \sum_{\mathbf{k},a,\sigma} (\epsilon_{\mathbf{k},a} - \epsilon_a) c_{\mathbf{k},a,\sigma}^\dagger c_{\mathbf{k},a,\sigma},
\]

where \( \epsilon_{\mathbf{k},a} \) label the five \( d \) bands, and \( \epsilon_a \) denote the band energies. The inter-orbital splitting arises from the real crystal field (of \( S_4 \) symmetry in Fe-pnictides), which lifts the five-fold degeneracy of the atomic \( d \)-shell. This gives the two hole- and two electron-like pockets, as apparently observed by de Haas van Alphen (dHvA) studies.

However, a direct comparison between LDA results and the PES/XAS experiments (which must be considered together when a comparison of the theoretical spectral function is attempted) shows substantial mismatch between theory and experiment. Related discrepancies are found in optical studies where the actual plasma frequency, \( \omega_p \), is 2–3 times smaller than the LDA prediction. Neither can the high \( (O(\text{m}\Omega\text{-cm})) \) resistivity be understood within an almost band-like (free electron) picture. Also, the dHvA study reveals that the LDA bands need to be shifted by 0.2 eV to get a proper fit with experiment. Further, the effective masses are enhanced by a factor of 2–3 over their LDA values (this agrees with the renormalization of the plasma frequency found in optics). Taken together, these features strongly suggest sizable electronic correlations, which, moreover, are also exhibited by a host of other, known, correlated metals.

Theoretically, while LDA (LDA+U) generically accounts for ground state properties of weakly (strongly)
correlated systems, their inability to describe excited states (and hence the charge and spin dynamics) in correlated systems is well-documented. Marrying LDA with DMFT opens the way toward resolving this shortcoming of traditional band structure approaches, and LDA+DMFT has proven successful in describing physical properties of various correlated materials in terms of their correlated electronic structures.

The discussion above clearly shows that incorporation of strong, multi-orbital electronic correlations is a requirement for a proper description of Fe pnictides. The interaction part is given by,

\[ H_{\text{int}} = U \sum_{i,a} n_{ia \uparrow} n_{ia \downarrow} + U' \sum_{i,a \neq b, \sigma, \sigma'} n_{ia \sigma} n_{ib \sigma'} - J_H \sum_{i,a,b} S_{ia} \cdot S_{ib}, \]

where \( n_{a \sigma} = c_{a \sigma}^\dagger c_{a \sigma} \) and \( S_a \) are the fermion number and spin density operators for an electron in orbital \( a \). We take \( U \approx U' + 2J_H \), as is commonly known for TMO. The relevance of strong correlations in Fe-pnictides has been recognized by several authors. While these works explicate the important role of multi-orbital (MO) correlations (in particular, the sensitivity to \( J_H \)) other works conclude that correlations are weak. This is a highly relevant, and open, issue in the field of Fe-pnictides and their SC: are they weakly correlated, itinerant metals, with a conventional, BCS-like instability to SC, or are they strongly correlated metals, giving way to SC via a non-BCS-like instability? A detailed comparison with extant experimental results should go a long way toward resolving this important issue.

Here, guided by good success obtained in a theory-experiment comparison of one-particle spectra in our previous study, we use LDA+DMFT to compute the detailed optical response in the “normal” state of La- and Sm-based Fe-pnictides. We solve \( H = H_0 + H_{\text{int}} \) within multi-orbital (MO) DMFT. In this study, MO-IPT is employed as the “impurity solver” to solve the impurity model of DMFT. Though not numerically “exact”, it has been shown to be quantitatively accurate for a wide range of correlated \( d \)-band materials. If only the FeAs layer states are relevant in Fe-pnictides, we expect our work to provide a generic picture of charge dynamics in Fe-pnictides. We find excellent quantitative agreement with both, the one-particle spectral data (PES/XAS) as well as two-particle data (reflectance) for the La-based Fe-pnictide. Based on this, we argue that Fe-pnictides should be viewed as strongly correlated, MO systems, with incoherent low-energy behavior and describe the optical response of both La- and Sm-based Fe-pnictides in detail. Implications of our work for the high-\( T_c \) SC in Fe-pnictides are touched upon, and intriguing similarities (and differences) with cuprates are highlighted.

Starting with the five Fe \( d \)-orbitals, we use MO-DMFT to extract the correlated spectral functions for the five \( d \)-orbitals. We choose values of \( U = 4.0 \) eV, \( J_H = 0.7 \) eV and \( U' \approx (U - 2J_H) = 2.6 \) eV, as employed in our earlier work. These are shown in Fig. 2 for La-based Fe-pnictide, for three values of electron doping, so that \( n_{\text{total}} = \sum_a n_a = (6 + x) \), with \( x = 0.1, 0.2, 0.3 \), along with the respective LDA DOS. Electronic correlations are seen to lead to dramatic and interesting modifications of the LDA spectra:

(i) the spectra describe an incoherent, non-FL metal for each of the \( d \)-bands, with orbital dependent low-energy pseudogap features. Correspondingly, the imaginary parts of the self-energies (not shown) show devi-
ations from the $-\omega^2$ form at small $\omega$, being consistent instead with a sub-linear $\omega$-dependence, along with a \emph{finite} value at $E_F = 0$, as also seen in our earlier work.\(^{25}\)

(ii) In striking contrast to the LDA band structures, the LDA+DMFT band structure shows that multi-orbital electronic correlations “self-organize” the spectral functions. While the $xy$-orbital DOS shows the maximum itinerance, and has a shape distinct from the others, the much more localized $xz, yz, x^2-y^2, 3z^2-r^2$-orbital-DOS are seen to closely resemble each other with regard to their lineshapes. Dramatic spectral weight transfer (SWT) over large energy scales $O(5.0)$ eV is also apparent in the results. In our MO-DMFT calculation, strong, incoherent inter-orbital charge transfer leads to dramatic spectral weight redistribution between the different $d$-orbital DOS. This is a characteristic also exhibited by other, correlated, MO systems,\(^{37}\) and points to the relevance of MO correlations in the Fe-pnictides.

(iii) There is no OS metallic phase for our choice of parameters, and \emph{all} $d$-orbital DOS cross $E_F$. The DMFT results are sensitive to changes in $U, U'$ for fixed $J_H$, and our results describe a metal very close to the OS-metallic one, which occurs for $U \gtrsim 5.0$ eV.

Very similar features have been reported by us for Sm pnictides in an earlier study.\(^{25}\) This is shown in the lower panel of Fig. 2. Given that the LDA bands for Sm-based Fe-pnictide are slightly wider than for La-based Fe-pnictides, we expect localization-like features to be more enhanced in La-based Fe-pnictides within a Mott-Hubbard picture, as is indeed seen in the comparison. These results imply that strong, MO correlations may have a \emph{generic} consequence of self-organizing the correlated spectra, an observation not readily seen in the LDA DOS. This may have important consequences, and, for example, could be of aid when one seeks to construct effective \emph{correlation} based models.

In Fig. 3, we compare our LDA+DMFT results with extant photoemission (PES) and X-ray absorption (XAS) data for LaO$_{0.93}$FeAsF$_{0.07}$\(^{38,39}\). Since only the five $d$-bands have been included in the LDA+DMFT, we restrict ourselves to the energy window (which, however, is rather wide) $-0.6 \leq \omega \leq 1.2$ eV around $E_F$ (this is the region where only the five $d$-bands dominate in the LDA). Clearly, excellent quantitative agreement with both PES and XAS results is obtained. In particular, the low-energy pseudogap is faithfully reproduced, as is the detailed form of the lineshapes. Taken together with our earlier results on SmO$_{1-x}$FeAsF$_x$\(^{25}\), this strongly suggests that the FeAs states with sizable $d$-band electronic correlations are a universal feature of Fe-pnictides.

In particular, a noteworthy fact is that for \emph{both} Fe-pnictides, a low energy kink at approximately $15.0-25.0$ meV, along with a pseudogap, and strongly asymmetric incoherent features at higher energies (at $-0.28$ eV in PES and at $0.6$ eV in XAS) are clearly resolved. Remarkably, our LDA+DMFT calculation reproduces \emph{all} these features in excellent agreement with both PES and XAS results. The low-energy kink is interpreted as arising from low-energy, collective inter-orbital fluctuations, as discussed earlier in detail.

Additionally, two more interesting features are also visible from Fig 3. First, a good “fit” between the experimental and LDA values of the Fermi energy is achieved by shifting the LDA spectrum downwards by $0.15$ eV. The need for such a shift of LDA DOS in this context has already been noticed earlier\(^{38}\) and attributed to correlation effects. Hitherto, their quantification has not been undertaken. Here, this already arises self-consistently in the MO-DMFT from the MO-Hartree shift mentioned above, bringing the LDA+DMFT value of $E_F$ in very good agreement with experiment. Second, as we will estimate below in optical analysis, the effective plasma frequency is reduced by a factor of $2-3$ over its LDA value. This translates into an \emph{average} effective enhancement of the band (LDA) mass as $2-3m_0$, where $m_0$ is the bare LDA mass. \emph{Both} these observations are completely consistent with the dHvA results, where very similar estimates for the band shift as well as the effective mass were extracted.\(^{33}\) In addition, the latter is also consistent with the $2-3$-fold enhancement in the $\gamma$ co-efficient of the low-$T$ specific heat in LaO$_{1-x}$FePF$_x$.\(^{40,41}\) Taken together, these results constitute a consistent, \emph{quantitative} rationalization of basic one-particle responses in both (La- and Sm-based) pnictides.
IV. OPTICAL CONDUCTIVITY USING LDA+DMFT

We now study the optical conductivity of both, doped LaOFeAs and SmOFeAs using the LDA+DMFT propagators for all $d$-orbitals. In $D = \infty$, the computation of the optical conductivity simplifies considerably. This is because the irreducible vertex functions entering the Bethe-Salpeter equation for the evaluation of the current-current correlation function vanish exactly in this limit. Thus, the optical response is directly evaluated as convolution of the DMFT propagators. For MO-systems, the general expression for the real part of the optical conductivity is given by

$$
\sigma_{ab}'(\omega) = \frac{2\pi e^2 \hbar}{V} \sum_{k} \int d\omega' f(\omega') - f(\omega + \omega') \frac{\omega}{\omega}
\times Tr[A_k(\omega' + \omega)v_{k,a}A_k(\omega')v_{k,b}],
$$

with $a$, $b$ labelling the various orbitals used in the DMFT calculation. $A_k(\omega)$ is the one-particle spectral function, a matrix in the orbital sector, and $v_{k,a} = \langle k|P_a|k \rangle$ is the fermion velocity in orbital $a$. The corresponding matrix element of the momentum, $P_a$, weights the different transitions, and is determined by the band structure. Estimation of the $v_{k,a}$ for Fe-pnictides is especially difficult, where, in addition to the $d$-states (which can be written in localized, Wannier-like basis sets), one also has the much more delocalized As $p$-states to contend with. Hence, we simplify our analysis by replacing this matrix element by a constant, $v_{k,a} = \langle k|P_a|k \rangle = v_{a}$. Further, we restrict ourselves to intraband transitions. Both these approximations will turn out to be justified later. With these simplifications, the optical conductivity is written as

$$
\sigma_{ab}'(\omega) = \delta_{a,b} v_a^2 \frac{2\pi e^2 \hbar}{V} \sum_{k} \int d\omega' f(\omega') - f(\omega + \omega') \frac{\omega}{\omega}
\times A_{k,a}(\omega' + \omega)A_{k,a}(\omega'),
$$

where

$$
A_{a}(k,\omega) = -\frac{1}{\pi} Im \left[ \frac{1}{\omega - \epsilon_{k,a} - \Sigma_{a}(\omega)} \right]
$$

is the fully renormalized one-particle spectral function for orbital $a$, and $\Sigma_{a}(\omega)$ is the corresponding one-particle self-energy. The total reflectivity, $R(\omega) = \sum_{a} R_{a}(\omega)$, can be computed using

$$
R_{a}(\omega) = \left| \frac{\sqrt{\epsilon_{a}(\omega)} - 1}{\sqrt{\epsilon_{a}(\omega)} + 1} \right|^2,
$$

with

$$
\epsilon_{a}(\omega) = 1 + \frac{4\pi i \sigma_{a}(\omega)}{\omega}
$$

being the complex dielectric constant.

Using the Kramers-Krönig (KK) relations, a detailed analysis of the reflectivity, $R(\omega)$, and the optical conductivity can be readily carried out for the normal state. In addition, an extended Drude analysis of the results shines light on the nature of the strong renormalizations caused by MO electronic correlations. In particular, estimation of the frequency-dependent carrier lifetime, $\tau(\omega)$, and effective mass, $m^{*}(\omega)$, for each orbital state yields microscopic information on the mechanism of incoherent metal formation. Finally, the electronic “glue” responsible for pairing is estimated therefrom as $\tau^{2}

$$
F_{a}(\omega) = \alpha_{a}^2 F_{a}(\omega) = \frac{1}{2\pi} \frac{d^2}{d\omega^2} \left( \frac{\omega}{\tau_{a}(\omega)} \right)
$$

whence microscopic information concerning the detailed structure of the pairing interaction is obtained.

V. RESULTS FOR ELECTRODYNAMIC RESPONSE

We now describe our results. In doing so, we adopt the following strategy:

(i) we use our LDA+DMFT results for doped LaOFeAs, which give a very good description of the one-particle spectral features, Fig. 2 as discussed above. Using the DMFT propagators, we compute the intraband optical conductivity of LaO$_{1-x}$FeAsFe$_x$. Excellent quantitative agreement with extant reflectivity data as measured is obtained, and, building upon this agreement, we describe the optical response (i.e. optical conductivity, dielectric constants, plasma frequency, ac penetration depth) in detail.

(ii) Given that the observation that the electronic structure of the Fe-pnictides is determined by the electronic states in the FeAs layers, we use our DMFT results for both La- and Sm-based Fe-pnictides to compute the normal state electrodynamics in the correlated metal. We provide the first theoretical estimates of the anisotropic carrier lifetimes and effective masses as a function of frequency. These results show, in accord with the incoherent metal classification of single layer Fe-pnictides, that their normal state cannot be described within FL theory.

In Fig. 3 we show the theory-experiment comparison for the reflectivity of LaO$_{0.6}$FeAsFe$_{0.1}$. The experimental result was taken from earlier work. Quite remarkably, excellent semiquantitative agreement is clearly visible for $U = 4.0$ eV, $U' = 2.6$ eV, and $J_H = 0.7$ eV in LDA+DMFT. To highlight the importance of strong electronic correlations, we have also plotted theoretical results for smaller, unrealistic values of $U = 2.0$ eV, $U' = 1.3$ eV and $U = 1.1$ eV, $U' = 0.7$ eV. Clearly,
in all respects, the agreement gets worse with decreasing $U, U'$, strongly supporting the strong correlation-based view. This excellent quantitative agreement with both one- and two-particle spectra in the normal state of LaO$_{1-x}$FeAsF$_x$ encourages us to make a deeper analysis of transport properties for both La- and SmO$_{1-x}$FeAsF$_x$.

Using Eq. (7), we have computed the optical conductivity, which is shown in Fig. 5 for all $d$-orbitals for both Fe-pnictides. Anisotropic responses, dictated both by LDA band-structure, as well as by correlation effects (see below) are clearly visible. A very interesting aspect of the results is the observation of strong incoherent features in $\sigma_a(\omega)$: a Drude-like peak, with very small weight, exists only in $\sigma_{xy}(\omega)$, and is even smaller, almost vanishing, in the $xz, yz$ optical response. For all other orbitals, the optical response is totally incoherent, with distinct non-Drude contribution (also see the carrier mass/lifetime results below). Large scale SWT across huge energy scales $O(4.0)$ eV with doping is also explicit in the results. In the MO-DMFT, this SWT is driven by the dynamical correlations associated with large on-site interactions $U$ and $U'$: the latter causes inter-orbital SWT on the observed scale, and is intimately linked with underlying “Mottness” in the MO model. The orbital resolved optical conductivity shows a distinctly non-Drude component, along with a very slow decrease with increasing $\omega$ up to high energy, $O(3.0)$ eV. This is observed clearly in Fig. 5 for both pnictides. At higher energies, one expects both, the inter-orbital transitions, as well as those between the bands neglected within the DMFT to start contributing to $\sigma_a(\omega)$. Thus, one should expect to find good agreement with experiment up to $\omega \approx O(3.0)$ eV. It is rather satisfying to notice that precisely the above features, i.e, non-Drude low-energy part, a slowly decaying (in $\omega$) contribution at higher energies, and large-scale SWT with doping, have indeed been observed in Fe-pnictides. These imply that Fe-pnictides should be considered as strongly correlated systems, in the proximity of a MI state.

Using Eq. 7, we have computed the optical conductivity of LaO$_{1-x}$FeAsF$_x$ for $x = 0.1, 0.2, 0.3$, within LDA+DMFT. Apart from the very small quasi-coherent component in $\sigma_{xy}(\omega)$, all other orbital components exhibit incoherent non-FL responses, with clear wipe-out of the “Drude” response at low-energy. Bottom panel: Comparison between the orbital resolved optical spectra for doped La- and Sm-based Fe-pnictides, showing very similar responses in both cases.
estimated the average plasma frequency from the sum rule,

$$\int_0^\infty \sigma(\omega) d\omega = \frac{\varepsilon_p^2}{4\pi}, \quad (12)$$
yielding $\omega_p = 0.76$ eV, in excellent agreement with the experimental estimate of 0.68 eV for LaO$_{1-x}$FeAsF$_x$ with $x = 0.1$. This is a renormalization of a factor of 3 relative to the LDA estimate. For comparison, we have also computed $\omega_p$ with reduced $U, U'$, whence $\omega_p$ increases smoothly toward its LDA value (this is also visible from the reflectivity curves, where the kink moves to higher energy with decreasing $U, U'$).

Using the extended Drude parametrization allows us to estimate the frequency-dependent transport scattering rate, $\tau^{-1}(\omega)$, as well as the dynamical mass, $m^*(\omega)$. In Figs. 6 and 7 (top panels), we show these quantities for each orbital, $a$, as a function of doping. Distinctive non-FL features are clearly evident. We emphasize that these results are valid in the symmetry unbroken metallic state, i.e., without SDW or SC order: this is the case above $T_c$ in doped Fe-pnictides for $x \geq 0.1$. Both $\tau^{-1}$ and $m^*$ show distinctly orbital-selective non-FL behaviors. With the exception of the $xy$ orbital, $m^*(\omega)$ for the other ($x^2 - y^2$, $xz, yz, 3z^2 - r^2$) orbitals continues to increase in a power-law-like fashion, or in a fashion consistent with the onset of incoherent pseudogap behavior down to lowest energy. Correspondingly, the respective scattering rates clearly exhibit a sublinear $\omega$ dependence (with anisotropic, $\omega = 0$ values) at low energy. Interestingly, the DMFT optical spectra of both La and Sm-based pnictides show that the dominant low-energy “metallic” contribution comes from the $d_{xz,yz,xy}$ bands, while clear pseudogap response is manifest in the $d_{x^2 - y^2,3z^2 - r^2}$ channels: the latter are almost Mott localized. This observation is consistent with ARPES data, where the correlated spectral function is measured; extant results show broadened “quasiparticle” bands on $xy, yz, xz$ character crossing $E_F$. In our DMFT, only the “more metallic” $xy, yz, xz$ bands will then show up as quasicoherent bands crossing $E_F$, while, for the pseudogapped $x^2 - y^2, 3z^2 - r^2$ bands, the extremely large scattering rates (with a pseudogap) will obliterate these in ARPES.

It is instructive to analyze the differences between the optical spectra for La- and Sm pnictides. In the lower panels of Figs. 6-7, we explicitly show these. Clearly, the anisotropic pseudogap features discussed above are more pronounced for the La-based Fe-pnictide. To understand this difference, we recall that the LDA band widths for Sm-based Fe-pnictide are about $O(0.5)$ eV wider than those for La-based Fe-pnictide, an observation that is consistent with the higher chemical pressure induced by the smaller (Sm) ion in the former case. Hence, in our DMFT picture, the correspondingly narrowed $d$ orbitals for La-based Fe-pnictide will be closer to Mott localization vis-a-vis those for the Sm-based Fe-pnictide; this manifests itself in the observation of pseudogap signatures in $\tau^{-1}_a(\omega)$, $m^*_a(\omega)$ for La pnictide, while these are weaker for Sm pnictide. Apart from these material dependent differences, the aspect of large normal state incoherence is clearly reflected in the results for both pnictides.

Finally, we remark that, while such extended Drude analysis for the “single layer” Fe-pnictides remains to be done with single crystals, a non-FL scattering rate

![Graphical representation of orbital-resolved scattering rates](image-url)
VI. DISCUSSION

The lack of any Drude component in the low-energy optical response implies that the symmetry-unbroken metallic state above $T_c$ in the doped Fe-pnictides is not a FL, in the sense that the one-particle propagators exhibit a branch cut structure, rather than a renormalized pole structure, at low energies.

What is the microscopic origin of the non-FL features found in the DMFT solution? In MO systems, the orbital-resolved hopping matrix elements (diagonalized in the LDA) are very directional, being sensitive functions of orbital orientation in the real structure. Further, the $d$ bands are shifted relative to each other because of the action of the crystal field (of $S_4$ symmetry in Fe-pnictides), and the six $d$ electrons are distributed among all $d$ orbitals. In this situation, strong, MO correlations cause two, intimately linked changes:

(i) the static MO-Hartree shift, which depends upon the occupations of each orbital, as well as on the inter-orbital $U'$ and $J_H$, renormalizes the on-site energies of each orbital in widely different ways. In particular, it causes inter-orbital charge transfer between the various $d$-orbitals, self-consistently, modifying their energies and occupations. This effect is also captured in LDA+U approaches. Specifically, the lower-lying orbital(s) in LDA are pushed further down by the MO-Hartree shift, the amount of which is determined by their occupation(s) and by the values of $U'$, $J_H$ relative to their respective LDA band width(s), and to the bare crystal field splitting in LDA.

(ii) More importantly, the dynamical correlations associated with $U$, $U'$, $J_H$ results in a large-scale transfer of dynamical spectral weight. Small changes in the LDA band structure induced by (i) above (or by changes in external perturbations in general) induce large changes in SWT, drastically modifying LDA lineshapes.

(iii) Crucially, the renormalized Fermi energy is computed selfconsistently in DMFT by requiring consistency with the Freidel-Luttinger theorem; i.e., $E_F$ is computed by demanding that the renormalized Fermi surface encloses the total number of $d$-electrons in the system, as long as no broken symmetry states are considered.

Generically, as $U'$ increases ($J_H$ is usually fixed for a given $d$-state), the lower-lying subset of $d$-orbitals gets selectively Mott localized; the metallic phase is then the OS metal found recently in various contexts. Once this selective localization occurs within the DMFT, the low energy physical response is governed by strong scattering between the effectively Mott-localized and the renormalized, itinerant components of the matrix spectral function. The problem is thus effectively mapped onto a Falicov-Kimball type of model, as has been noticed in earlier work. Within DMFT, the itinerant fermion spectral function then shows a low-energy pseudogapped form, while the “localized” spectral function shows a power-law fall-off as a function of energy, as long as the renormalized $E_F$ is pinned to the renormalized orbital

is indeed extracted from the optical spectra for doped BaFe$_2$As$_2$. Based on our results, we predict that similar incoherence will characterize the normal state optical response of the single-layer Fe-pnictides as well. The sublinear-in-$\omega$ scattering rate is also consistent with the sublinear-in-$T$ dependence of the $dc$ resistivity in doped Fe-pnictides above $T_c(x)$. 

![FIG. 7: (Color online) Top panel: Orbital-resolved dynamical masses of LaO$_{1-x}$FeAsF$_x$ for $x = 0.1, 0.2, 0.3$, within LDA+DMFT. All orbital components exhibit strong $\omega$-dependence at low energy, in line with the incoherent optical responses. Only the mass for the $xy$ orbital carriers seems to approach a constant, correlation-enhanced value at low energy. For the others, the dynamical masses exhibit strong $\omega$ dependence up to low-energy, in full accord with the emergence of low-energy incoherent, or pseudogap-like features in their corresponding one-particle and optical lineshapes. Bottom panel: Comparison between the orbital resolved dynamical masses for doped La- and Sm-based Fe-pnictides, showing very similar responses in both cases. Notice the enhanced low-energy incoherence for the La-pnictide.](image-url)
energy of the localized orbital(s). This is understood from the mapping of the corresponding impurity model to that of the “X-ray edge”\(^\text{22}\) where the orthogonality catastrophe destroys FL behavior.\(^\text{46}\) The spectral functions then exhibit asymmetric continua (branch cuts) at low energy, instead of symmetric Abrikosov-Suhl Kondo resonance features, and the metallic phase is not a FL. This incoherence is mirrored in the optical responses in \(D = \infty\), since the optics is entirely determined by the full DMFT one-particle Green functions in this limit. This is entirely consistent with our results, and strongly suggests that effects akin to the orthogonality catastrophe, arising from strong, incoherent, inter-orbital scattering, produce the incoherent metal behavior in the “normal” state of Fe-pnictides.

This loss of one-particle coherence corresponds to drastic reduction of the carrier kinetic energy, and implies the irrelevance of one-particle terms in the RG sense.\(^\text{45}\) Interestingly, this clears the way for two-particle instabilities to take over as \(T\) is lowered; they pre-empt the non-FL behavior from persisting down to \(T = 0\). This could be either:

(i) the \(\mathbf{q} = (\pi, 0)\) SDW for \(x < x_c\). This is in fact further reinforced by the near-nested character of the electron- and hole Fermi pockets in the Fe-pnictides, already visible in weak coupling RPA calculations.\(^\text{14,48}\) The SDW instability at \(x = 0\) is then interpretable as an instability in the particle-hole channel, aided by near FS nesting. That AF-SDW survives the lack of such nesting features away from \(x = 0\) is an observation which favors a strong coupling scenario. An intermediate-to-strong coupling version of a similar instability to exactly the same state results from the LDA+DMFT work of Haule et al.\(^\text{20}\) A strong coupling method as used here will yield the same AF instability, in analogy with one-band Hubbard model studies, where the AF ordered state at half-filling remains the Neel ordered state, evolving from the Slater type to the Mott-Hubbard type as \(U/t\) is increased. Though weak-coupling RPA approaches, valid for small \(U/t\), can indeed give the correct magnetic ground states for \(U \ll W(= 2zt)\), the normal state incoherence characteristic of Fe-pnictides, which are now identified to be in the intermediate coupling limit \((U \simeq W)\), is beyond their scope. This is because the incoherent part of \(G_\mathbf{k}(\mathbf{k}, \omega)\) is completely neglected there, and one deals with propagators having only a coherent QP pole structure at low energy. This is valid for small \(U\), but not for \(U > W\), the non-interacting bandwidth.

(ii) An unconventional SC for \(x > x_c\). This corresponds to an instability in the particle-particle channel. Independent of the precise order parameter symmetry, a matter of intense debate,\(^\text{3,6,8,9}\) the observation of small superfluid density, short-coherence length, large \(2\Delta/kTc\) ratios, along with large energy scale changes in optical response across \(T_c\), are all hallmarks of a SC closer to the Bose condensation limit, rather than the weak coupling BCS limit.

Our findings are in accord with Si et al.\(^\text{2}\) and Haule et al.\(^\text{20}\), who, along with Baskaran,\(^\text{46}\) were the first to recognize the strong coupling aspect of Fe-pnictides. On the other hand, several works address both AF and SC within weak coupling scenarios.\(^\text{14,48}\) In the latter, the “normal” state above \(T_c\) is a FL metal, and SC arises via a BCS like instability of this MO (multi-band) FL.

In the strong correlation limit, however, the “normal” state is itself incoherent, and so there are no FL-like QPs to pair up into usual BCS-like Cooper pairs. In other words, SC must then arise as an instability of an unusual metallic state without FL QPs, or, to rephrase it, directly from overdamped, collective multi-particle modes. The frequency-dependence of the self-energy is important in the latter case, and consideration of the instability of such an incoherent state to the SC state leads to a strongly frequency-dependent SC gap function. In such a “strong coupling” picture, the physical response functions in the SC state are controlled by both, the symmetry of the SC order parameter, as well as the strong, \(\omega, T\) dependent damping originating in the incoherent “normal” state.

Observation of features such as the absence of the Hebel-Slichter peak in the NMR \(T_1^{-1}(T)\)\(^\text{3,5}\) and the large scale modification of the optical spectral weight across \(T_\text{c}\)\(^\text{22}\) in the Fe-pnictides are strongly suggestive of such a strong coupling scenario. These features are again reminiscent of cuprates,\(^\text{19,44}\) where the role of “normal” state (non-FL) incoherence is well documented. To make their role in the Fe-pnictides more explicit, we use our optical results to show the pairing “glue” function for Fe-pnictides in Fig.\(^\text{S}\) In line with the conclusions extracted from the analysis of the incoherent optical conductivity above, \(\mathcal{F}(\Omega)\) shows interesting features. We find

(i) a two “peak” structure, with both peaks strongly broadened by incoherent scattering. We emphasize that this broad, two-peak structure arises from the incoherent one-particle propagators, and represents a multiparticle electronic continuum. This could be interpreted as overdamped “bosonic” modes, if one associates the short ranged, strongly coupled spin-orbital modes with the incoherent, short-distance components of the conventional bosonic modes used in the itinerant descriptions. It is interesting to notice that similar features, namely, strong non-FL signatures in optics, as well as a strongly damped, two-peaked, low-energy continuum is also characteristic of high-\(T_c\) cuprates up to optimal doping.\(^\text{13,49}\) Thus, our results show that SC arises from an incoherent normal state, and that coupling carriers to an incoherent electronic continuum pairs them up in the SC. Hence, we propose that the underlying Mott-Hubbard physics known to underpin the anomalous responses in cuprates is also at work in the Fe-pnictides.

(ii) All \(d\)-orbital components show up in \(\mathcal{F}_\mathbf{a}(\omega)\), albeit anisotropically. This supports a MO (multi-band) origin for SC pairing in Fe-pnictides. Several interesting features are visible upon close scrutiny: the “glue” function is larger for those (orbitals) bands which are closer to Mott localization, as seen by comparing the respective curves in \(\mathcal{F}_\mathbf{a}(\Omega)\) and \(\rho_c(\omega)\), while the most “itinerant”
channels. In the doped case, lack of nesting features in the electron-like and hole-like Fermi sheets suppresses the \( q = (\pi, 0) \) SDW found for \( x = 0 \), leaving multiband SC as the only relevant two-particle instability. In such a MO-SC, opening up of an orbital-dependent gap should be linked to orbital-dependent coupling of the carriers to the electronic “glue” via \( \mathcal{F}_a(\omega) \): remarkably, a very recent indeed shows exactly this feature.\textsuperscript{20}

This agrees qualitatively with our expectations from a strongly orbital-dependent “glue” function, as derived above. It is also interesting to note that a recent ARPES study on \((\text{Sr/Ba})_{1-x}\text{K}_x\text{Fe}_2\text{As}_2\)\textsuperscript{54} also finds quasiparticle kinks in the quasiparticle dispersion in the binding energy range from 15 meV to 50 meV, again reminiscent of what is observed in high-\(T_c\) cuprates,\textsuperscript{22} but also in three dimensional, correlated systems like \(\text{SrVO}_3\).\textsuperscript{50}

The latter fact points to its connection to underlying Mott-Ness characteristic of a correlated system. In our DMFT, we recall that the orbital-resolved DOS show low-energy kinks precisely in the 15 – 50 meV range (see Fig. 7). These are attributed to low-energy, collective, inter-orbital fluctuations\textsuperscript{23} and we have shown that the resulting LDA+DMFT DOS gives excellent quantitative agreement with the normal state kink-like feature in angle integrated \(\text{PES}\).\textsuperscript{24} Based on our calculation, we propose that an ARPES measurement done for \((\text{La/Sm})\text{O}_{1-x}\text{FeAsF}_x\) should uncover kink structure(s) in a similar low-energy (20 meV) range.

Whether additional density-wave instabilities may also interfere with SC is an interesting issue. Two-band model studies\textsuperscript{48,55} do suggest additional channels involving nematic or current instabilities: whether they can seriously compete with SC or remain sub-leading in the full five-band model, is still unclear. In any case, our analysis shows that consideration of all \(d\)-orbitals is necessary for a proper microscopic description of multi-band SC in Fe-pnictides. We leave the detailed consideration of the instability of the MO, incoherent metal found here to a MO SC for future consideration.

A brief discussion of the similarities and differences between cuprates and Fe-pnictides is in order at this point. The predominance of normal state incoherence in cuprates is well-documented by now\textsuperscript{20} and its link with the strong on-site electronic correlations is well known. In particular, strong non-FL features (with a branch cut form of the one-particle propagator, \(G(\mathbf{k}, \omega)\)) in ARPES, \(dc\) and \(ac\) transport, magnetotransport, as well as in magnetic fluctuations bears this out in a very remarkable way. Up to optimal doping, the cuprates are not describable in terms of the Landau FL picture, and the role of strong Mottness and short-ranged AF spin correlations in this context is recognized. In the underdoped cuprates the instability to the \(d\)-wave SC state is quite far from the weak-coupling BCS variety: large-scale redistribution of spectral weight across \(T_c\) as well as strong vortex liquid fluctuations, short SC coherence lengths, and small superfluid stiffness, among other observations, put this transition closer to the Bose condensed limit.

**FIG. 8:** (Color online) Top panel: Orbital-resolved “glue” functions for \(\text{LaO}_{1-x}\text{FeAsF}_x\) for \(x = 0.1, 0.2, 0.3\), within LDA+DMFT. \textit{All} orbital components contribute, albeit anisotropically, at low energy. This suggests that the instability to superconductivity in Fe-pnictides will involve multiple bands. The lack of any sharp feature shows that the “glue” is an overdamped electronic continuum (see text). The two-peak structure at low energy is reminiscent of what is seen in high-\(T_c\) cuprates, and has a multi-orbital character. Bottom panel: Comparison between the “glue” functions for doped La- and Sm-based Fe-pnictides, showing similar incoherent electronic continuum features in both cases.
Many of these features, like normal state incoherence, along with pseudogap behavior in both charge and spin fluctuations, are also characteristic of Fe-pnictides. Further, in single-layer Fe-pnictides, the superfluid density is small, the upper-critical fields, $H_{c2}$, is high, the SC in-plane coherence length is short ($\xi_{\text{pair}} < 20 \text{ Å}$), and appreciable redistribution of spectral weight across $T_c$ is visible. These similarities then strongly support the strong correlation-based view for Fe-pnictides as well.

There are noticeable differences between the cuprates and the Fe-pnictides. First, SC in cuprates most likely involves a single, strongly $p-d$ hybridized band with strong electronic correlations, and arises upon doping a Mott-Hubbard insulator with AF order. In contrast, SC in Fe-pnictides is most probably of the multi-band variety, and arises upon doping a very bad metal, which may be close to a Mott-Hubbard insulating state. This means that the microscopic electronic “glue” for pairing in both cases will be quite different. Nevertheless, in view of the underlying relevance of Mottness in both cases, one may expect more similarities in the structure of the SC instability in both cases. It is more likely, given the explicit MO situation in Fe-pnictides, that additional competing instabilities may be at work. In particular, the nematic and current instabilities, which have been invoked as competitors of $d$-wave SC in cuprates, might also play a role here. As remarked early by Baskaran, it is possible that being able to think about situations where these competing instabilities could be suppressed can push up the SC $T_c$ in Fe-pnictides to even higher values.

Our analysis here has been carried out for the symmetry-unbroken metallic state of the Fe-pnictides. At low $T$, this incoherent state becomes unstable to either AF-SDW order with $Q_{SDW} = q = (\pi, 0)$ or to SC order, depending on $x$, though some studies also suggest coexistence of the two orders. As discussed in literature, the AF-SDW state involves strong geometric frustration (GF) in the inter-orbital hopping matrix elements. Characterization of magnetic fluctuations has indeed been carried out, both in the strong coupling ($J_1 - J_2$ Heisenberg model) as well as within weak coupling HF-RPA work. Observation of features akin to high-Tc cuprates found experimentally, as discussed above, put the Fe-pnictides into the strongly correlated category, though not so strongly correlated as cuprates, which are doped Mott insulators. While the fact that we are able to describe both the one-electron responses and the reflectivity of La-pnictide strongly suggests that LDA+(MO)DMFT is adequate for a quantitative description of these correlation effects, we expect geometrical frustration effects to become relevant at low $T < T_N(x)$, at least for the SDW phase. In view of the fact that the spatial extent of correlations is short in GF systems, we remark that the dynamical effects associated with these short-ranged magnetic correlations may not change the above results substantially. They will certainly not modify them qualitatively; indeed, one would expect that additional consideration of the dynamical effects of such short-ranged, strongly frustrated couplings ($J_1, J_2$ with $J_2/J_1 \approx O(1)$) would push the almost totally incoherent normal state derived above even more toward incoherence.

VII. CONCLUSION

In conclusion, we have studied the normal state electrodynamic response of two Fe-pnictides, La$_{1-x}$FeAsF$_x$ and SmO$_{1-x}$FeAsF$_x$, within the LDA+DMFT formalism. Armed with the very good agreement with one-electron responses (PES and XAS) between experimental and LDA+DMFT spectral functions, we also find very good quantitative agreement with published reflectivity data on LaO$_{1-x}$FeAsF$_x$. Building upon these agreements, we have studied the optical response in detail. We find an incoherent optical response, with strongly $\omega$-dependent effective masses and transport lifetimes (scattering rates) at low energy. These features are linked to the incoherent, near pseudogap-like features found in the orbital resolved, one-particle spectral functions in LDA+DMFT. The very good agreement found between theory and experiment for both pnictides is strong evidence for the relevance of “Mottness”, i.e., to proximity of the normal state of Fe-pnictides to a correlation-driven Mott-Hubbard insulating state. Further, based on an estimation of the “glue” function, we propose that this should be understood as arising from a multi-particle electronic continuum, which could also be interpreted in terms of an overdamped “bosonic” glue. Finally, all $d$-orbitals should contribute to SC pairing, albeit anisotropically, and one should have an orbital-dependent, multiple-gap SC. It is an interesting task to investigate the low-$T$ instabilities of this incoherent metallic state: we leave this for the future.

L.C. thanks S.-L. Drechsler for discussions. S.L. acknowledges ZIH Dresden for computational time. M.S.L. thanks the MPIPKS, Dresden for financial support.

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