Modification on Shahad.A.H Distance for Images processing

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ABSTRACT:

In our paper we presented a suggested method for encoding images based mainly on Shahad.A.H distance, and will name it modification of on Shahad.A.H (M Sh .AH) and Compare with Euclid distance and distance Shahad.A.H The rate of error ratio between the original images and the methods presented was calculated and indicated that the modified method was the best in terms of performance evaluation criteria PSNR, SSIM, COR, NPCR, RMSE, our aim of this paper to develop Shahad.A.H To effectively hide image features. Data base that independent in this paper (50 images) of different formats (.png,.bmp,.tif, .gif,.jpg,) and multi types (color, gray) images and In paper MATLAB® 2014 software is used in the computer programming.

Keywords: Image processing, Image encryption, Distance Measure, Shahad.A.H Distance.

1.INTRODUCTION

The data can be protected either text, image and video by encrypting and transmitting information using mathematical equations and modern software technologies[1]. Encryption Image is one of the important tool for carrying information by applying encryption process information is encoded by the authorized persons schemes have been increasingly studied to meet demand for real time method secure image transmission over private or public networks[2].

There are so many different features used to measure image encryption range by find and analyzing Mathematical parameters are very important. The following values must be consider are key space, histogram analysis, correlation coefficient analysis, number of pixels change rate, PSNR, and MSE[3]. The paper is divided into 7 sections after the introduction comes the second section is the most prominent distances used and the third section represents the proposed method, Section 4 outlines a set of important definitions and terms that will be used in the paper Section 5 Experiments and Results, While a description of the performance criteria in Section 6. The 7th and final section means the conclusions.

2.MATERIALS AND METHODS

In this section we discuss the definitions of distance measures:

Distance in matric space:

Suppose we have the set called Y, a function f : Y × Y → R is called distance on Y if ∀ s, a ∈ Y, then:

- l(s, a) ≥ 0 (non-negativity)
- l(s, a) = 0 ⇔ s = a (symmetry)
- l(s, a) = l(a, s) (reflexivity)

A most common distance measures:

Euclidean distance [5]:

\[ D_{\text{Euclidean}}(x_1, x_2) = \sqrt{\sum_{i=1}^{d}(x_{1i} - x_{2i})^2} \] (1)

Shahad .A .H DISTANCE [6]

Let X,Y are two points in two dimensional Euclidean spaces, the coordinates (x1, x2) with X, the coordinates (y1, y2) with Y.

The distance between X,Y is defined by:

\[ D(X,Y) = |1 - \tan^{-1}\sqrt{(x_1 - y_1)^2 + (x_2 - y_2)^2}| \] (2)

3. PROPOSED METHOD

For encryption image we used the inverse of Shahad .A .H distance method and multiplication with the mean value of all two pixels in image;

To apply the proposed method we must

1- find the Eq 2.
2-find the inverse of Eq 2.
3-find the multiplication between Eq2 and mean value of the coordinates \((x_1, x_2), (y_1, y_2)\) of X, Y respectively.

and we can calculated it by:

\[
D(X, Y) = \mu_{x,y} \cdot \left[1 - \tan \sqrt{\left(x_1 - y_1\right)^2 + \left(x_2 - y_2\right)^2}\right] ^2
\]  

we will call this method "M.Sh.A.H".

**SOME IMPORTANT DEFINITIONS**

**Peak Signal-To-Noise Ratio (PSNR)** [7].

\(s\) and \(z\) are two images (original image, test image) both of size \(M \times N\), for 256*256 images, Maximum intensity is 255(0 to 255).

\[
\text{PSNR } (s, z) = 10 \log_{10} \frac{255^2}{\text{MSE}(s, z)}
\]  

Where Mean square error (MSE) is defined by

\[
\text{MSE} = \frac{1}{mn} \sum_{i=1}^{m} \sum_{j=1}^{n} (s_{ij} - z_{ij})^2
\]  

\[
\text{Correlation Of Raw Scores} \ [8],[14].
\]

\[
\text{corr} = r = \frac{\Sigma(d_i - \bar{d})(s_i - \bar{s})}{\left[\Sigma(d_i - \bar{d})^2 \Sigma(s_i - \bar{s})^2\right] ^{1/2}}
\]  

where \(\bar{d}, \bar{s}\) are expected value of \(d_i, s_i\) respectively. When \(r = 1,-1\) that means the Correlation coefficient is very strong in (positive and in negative) respectively.

If \(r = 0\), then the Correlation coefficient is very week.

**structural similarity index[9].**

Structural similarity index defined by

\[
\text{SSIM}(r, o) = \frac{(2\mu_r \mu_o + c_1)(2\sigma_{ro} + c_2)}{(\mu_r^2 + \mu_o^2 + c_1)(\sigma_r^2 + \sigma_o^2 + c_2)}
\]  

and it contain 3 comparison functions known for: luminance comparison, contrast comparison, and structure comparison between two signals \(r\) and \(o\).

Where

\[
\mu_r = \frac{1}{m} \sum_{i=1}^{m} r_i, \quad \mu_o = \frac{1}{m} \sum_{i=1}^{m} o_i, \quad \sigma_r^2 = \frac{1}{m} \sum_{i=1}^{m} (r_i - \mu_r)^2, \quad \sigma_o^2 = \frac{1}{m} \sum_{i=1}^{m} (o_i - \mu_o)^2
\]  

Where \(\mu_r, \mu_o\) are the expected value of \(r\) and \(o\), and

\[
r = \left[\frac{1}{m-1} \sum_{i=1}^{m} (r_i - \mu_r)^2\right]^{1/2}, \quad o = \left[\frac{1}{m-1} \sum_{i=1}^{m} (o_i - \mu_o)^2\right]^{1/2}
\]  

\(c_1, c_2\) are the standard deviations of \(r\) and \(o\), respectively, and \(C_{ro}\) is the correlation coefficient between \(r\) and \(o\). when the denominators approach to zero Then constants \(c_1, c_2\), and \(c_2\) are used to stabilize the algorithm.

**Variance** [10].

If we have a set of values, then The variance this set, which denote by \(\sigma^2\), is defined as

\[
\sigma^2 = \frac{\sum (x - \bar{x})^2}{m}
\]  

where \(\bar{x}\) is the expected value, \(m\) is the NO. of data values, and \(t\) stands for each data value in turn. An alternative, yet equivalent formula, which is often easier to use is

\[
\sigma^2 = \frac{\sum t^2}{m} - \bar{x}^2
\]

**Root Mean Square Error** [11]:

\[
\text{RMSE} = \sqrt{\frac{\sum (x - \bar{x})^2}{m}}
\]

Where \(Z\) is the reference value and \(S\) is the approximation value.

**Histogram** [12].

\[
h(c_i) = n_i \quad c = 0,1,2, \ldots , l - 1
\]

\(c_i\): the c-th gray level.

\(n_i\): No. of times that the gray level \(w_i\) appears.

**Histogram Equalization** [13].

\[
Y_c = G(r_c) = \frac{\sum_{j=0}^{m_i} R_f(r_j)}{m_i} = \sum_{j=0}^{m_i} B_f(r_j)\]

\(0 \leq n_i \leq 1, L = 0,1,2, \ldots , l - 1\)

\(m_i\): the No. of times the \(r_c\)th gray level.

\(L\): NO. of gray levels.

\(B_f(r_j)\): the probability of the \(j^{th}\) gray level.

\(M\): the total No. of pixels.

**4.EXPERIMENTAL and RESULTS**

We will analyze in this section the effect of some of the prescriptions on the components of the image as follows:
Direct effect methods on original images.

**Fig 1**: Sample of images.

**Fig 2**: Effect of three methods on the original images.

Figure 2 shows the effect of the methods on the original images. It is shown that the modified method gives the best results and is the most effective in hiding the internal parts of the image.

**Histogram:**
Fig 3: effecting of histogram on a, b, c images with 3 methods of encryption.

Figure number 3 showed the effect of histogram criterion on original and encrypted images. For information read by the histogram Note that the histogram shows that the proposed method is that which yields a soft results, not as the other methods.

Histogram equalization:

Fig 4: Effecting of histogram equalization on a, b, c images with 3 methods of encryption.

Figure 4 exhibits the original image and the encrypted images, shows the difference between the images that had been encrypted by the previously mentioned methods and the image that is encrypted by modify Shahad. A.H. whatever the type of image, or indexed or bilateral, colored or gray, with the different extension of image, such that the modify method is more active than Shahad.A.H.

Variance (VAR):

Fig 5: variance of data on c image such that 1: original image, 2: Euclidean, 3: Shahad. A.H, 4: M Sh. A. H

Figure 5 The data is distributed in relation to their position in the image and confirms that the proposed method is the best in terms of the spread of data since the data are generated in a uniform and straight way, unlike the previous methods.

5. ANALYSES OF PERFORMANCE MEASURES

In this section we calculate the performance of the modification of Shahad. A.H method by using RMSE, (PSNR), Correlation Coefficient, and (SSIM) as show in Tables 1, 2, 3, 4.
Table 1: Showed the performance results of Peak Signal to Noise Ratio (PSNR).

| Code | Euclidean | Shahad. A.H | M Sh. A. H |
|------|-----------|-------------|------------|
| a    | 34.410723529726 | 21.214099226 | 29433 |
| b    | 27.606211306855975 | 14.05444934646 | 36073 |
| c    | 28.07972822916449278 | 14.936031384546947 | 6.27836405757673 |
| d    | 30.453610330001472 | 17.228685157508146 | 8.709087234894724 |

Table 2: showed the performance results of Structural Similarity Index (SSIM).

| Code | Euclidean | Shahad. A.H | M Sh. A. H |
|------|-----------|-------------|------------|
| a    | 0.961885818905327 | 0.539240026113141 | 0.010713913145305 |
| b    | 0.95549867515412 | 0.365320159361554 | 0.021645694690298 |
| c    | 0.952432517939255 | 0.22386140643410 | 0.011517031160739 |
| d    | 0.544248345418779 | 0.219796794704248 | 0.028977453430396 |

While Table 2 explain the results which demonstrated the efficiency of the modify Shahad. A.H method of coding with Structural Similarity Index (SSIM).

Table 3: showed the performance results of correlation coefficients.

| Code | Euclidean | Shahad. A.H | M Sh. A. H |
|------|-----------|-------------|------------|
| a    | 0.994020297197057 | 0.055800270219064 | 0.023943646224944 |
| b    | 0.991155562994657 | 0.048533897945003 | 0.0125415260903557 |
| c    | 0.990695563687809 | 0.0415436368988335 | 0.008775525576450 |
| d    | 0.994020297197057 | 0.055800270219064 | 0.023943646224944 |

Table 3 showed the performance results of correlation coefficients where that appear the modifying method is better than the other methods.

Table 4: showed the performance results of Root Mean Square Errors of the Shahad. A.H method and M Sh. A. H method where the last method had The highest error rate.

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6. CONCLUSION.

Note that the modified method is the best and most effective for all the criteria used, as well as is easy to use as it depends on finding the inverse of the old method and beating it with the expected value of coordinates. When looking at tables 1, 2, 3 and 4 note that the modified method gives an effective clear-cut evaluation of performance parameters. Where the table shows that the lowest value for PSNR is for the proposed method and this links to Table 4 where the relationship is inverse between PSNR and RMSE.

Table 2 illustrates the similarities between the original image and the images under the influence of the above methods. Where we note that the lowest amount recorded by the proposed method, as well as Table 3 shows that the weak correlation between the reference image and the image under the influence of the proposed method Compared to other methods s.t.less value belong to M SH.A.H method (i.e. good encryption).
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