HYPERVELOCITY STARS FROM A SUPERMASSIVE BLACK HOLE-INTERMEDIATE MASS BLACK HOLE BINARY

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\section*{ABSTRACT}

In this paper we consider a scenario where the currently observed hypervelocity stars in our Galaxy have been ejected from the Galactic center as a result of dynamical interactions with an intermediate-mass black hole (IMBH) orbiting the central supermassive black hole (SMBH). By performing 3-body scattering experiments, we calculate the distribution of the ejected stars’ velocities given various parameters of the IMBH-SMBH binary: IMBH mass, semimajor axis and eccentricity. We also calculate the rates of change of the BH binary orbital elements due to those stellar ejections. One of our new findings is that the ejection rate depends (although mildly) on the rotation of the stellar nucleus (its total angular momentum). We also compare the ejection velocity distribution with that produced by the Hills mechanism (stellar binary disruption) and find that the latter produces faster stars on average. Also, the IMBH mechanism produces an ejection velocity distribution which is flattened towards the BH binary plane while the Hills mechanism produces a spherically symmetric one. The results of this paper will allow us in the future to model the ejection of stars by an evolving BH binary and compare both models with \textit{Gaia} observations, for a wide variety of environments (galactic nuclei, globular clusters, the Large Magellanic Clouds, etc.).

\section{INTRODUCTION}

In the last decade, stars with extreme radial velocities have been discovered in the Galactic halo, the so-called hypervelocity stars (HVSs). They were first predicted by Hills (1988) as a natural consequence of the presence of a super massive black hole (SMBH) in the Galactic Centre (GC) that tidally disrupts binary stars approaching too close. However, they were not detected until 2005, when the first HVS was observed by Brown et al. (2005) escaping the Milky Way (MW) with a heliocentric radial velocity of \(\sim 700\text{ km s}^{-1}\). Gualandris et al. (2005) estimated an ejection velocity of \(\gtrsim 1000\text{ km s}^{-1}\) from the GC. Since then, \(\sim 20\) HVSs have been detected by the Multiple Mirror Telescope Survey out to a Galactocentric distance of \(\sim 120\text{ kpc}\) and with velocities of up to \(\sim 700\text{ km s}^{-1}\) (Brown et al. 2006, 2014). With an estimated ejection rate of \(10^{-6} - 10^{-4}\text{ yr}^{-1}\) (Yu & Tremaine 2003; Zhang et al. 2013), HVSs remain rare objects.

The European mission \textit{Gaia}\textsuperscript{1} has recently revolutionized astrometry and promised to discover new HVSs (Brown et al. 2015; Marchetti et al. 2017). The recent second data release (DR2) has provided positions, parallaxes and proper motions for more than \(\sim 1\) billion stars, along with radial velocities for \(\sim 7\) million stars (Gaia Collaboration 2018), thus offering an unprecedented opportunity to study the Galactic population of HVSs. Exploiting these data, Brown et al. (2018) showed that only the fastest B-type HVSs (radial velocities \(\gtrsim 450\text{ km s}^{-1}\)) have orbits surely consistent with a GC origin, while other HVSs have ambiguous origins. \textit{Gaia} new astrometry also allowed to reject most of the – already highly debated – late type HVS candidates (Boubert et al. 2018) and add evidence on the Large Magellanic origin of HVS3 (Erkal et al. 2018). As expected, discovery of new unbound HVSs has not yet happened because the sample of stars in DR2 with radial velocity is relatively too small and nearby for the rarity of HVSs and their expected distance distribution (Marchetti et al. 2018b). On the other hand, bound HVSs may have been found, although their metallicity and age make them hard to set apart from the halo star population (Hattori et al. 2018). The real treasure trove should be found in the rest of the catalogue with 5 dimension parameter space information, that requires more sophisticated data mining methods in order to select a manageable number of candidates to be spectroscopically followed up (Marchetti et al. 2017; Bromley et al. 2018).

Theoretically, many properties of the observed (and expected) HVSs remain poorly understood, including the dominant ejection mechanism. Several different mechanisms have been proposed to produce HVSs, besides the standard Hills binary disruption mechanism, still regarded as the favoured model. The main alternative was first proposed and discussed by Yu & Tremaine (2003), who suggested the ejection of HVSs as a consequence of star slingshots involving a massive black hole binary composed of the \(4 \times 10^6\text{M}_\odot\) SMBH already observed in

\textsuperscript{1} http://sci.esa.int/gaia/
the GC (i.e. SgrA*) and a putative secondary SMBH or intermediate mass black hole (IMBH) possibly delivered by infalling globular clusters due to dynamical friction in their host galaxy (Tremaine et al. 1975; Fragione et al. 2018a,b). A scenario subsequently explored in a series of papers by Sesana and collaborators, considering either the ejection of unbound stars (Sesana et al. 2006), or the erosion of a pre-existent bound stellar cusp (Sesana et al. 2008). Encounters with nearby galaxies (Gualandris & Portegies Zwart 2007; Boubert et al. 2017), supernova explosions (Zubovas et al. 2013; Tauris 2015), interactions of star clusters with single or binary SMBHs or IMBHs (Capuzzo-Dolcetta & Fragione 2015; Fragione & Capuzzo-Dolcetta 2016; Fragione et al. 2017) and the dynamical evolution of a disk orbiting the SMBH in the GC (Subr & Haas 2016) could all produce HVSs.

In this paper, we perform scattering experiments to determine the HVS ejection rate and also the distribution of their ejection velocities for both the Hills and IMBH binary companion scenarios. For the SMBH-IMBH binary scenario, we also calculate the evolution rate of its semimajor axis and eccentricity. Compared to previous works, we extend the scattering experiment parameter space to binary mass ratios as small as $10^{-4}$, and also consider the cases of corotating and counterrotating stellar nuclei. We correct an error in the calculations of the eccentricity evolution rate by Sesana et al. (2006). Another improvement is that for our scattering experiments we use the ARCHAIN algorithm, designed to accurately integrate the motions of arbitrarily tight binaries with arbitrary mass ratios (Mikkola & Merritt 2008).

The paper is organized as follows. In Section 2 we discuss various phenomena which could generate HVSs. In subsequent sections we numerically simulate two of those mechanisms: slingshot ejections by an SMBH-IMBH binary (Sections 3 and 4) and the Hills mechanism (Section 5). We conclude and discuss future work in Section 6.

2. MECHANISMS FOR PRODUCING HYPERVELOCITY STARS

In this section, we review the different mechanisms that could form hypervelocity stars in our Galaxy, along with their predicted observational signatures. The predicted observational properties expected for each mechanism are summarized in Table 1.

2.1. The Galactic Centre

The first mechanism proposed to produce hypervelocity stars is called the Hills mechanism (Hills 1988), and involves the disruption of binary star systems by a central super-massive black hole. As already discussed, a binary is required in order to provide a reservoir of negative orbital energy by leaving one of the binary components bound to the SMBH, such that a large positive kinetic energy for the ejected star is allowed by energy conservation. This mechanism can produce hypervelocity stars with velocities $\gtrsim 1000 \text{ km/s}$, depending on the SMBH mass and the properties of the stars (see Section 5).

This mechanism predicts an isotropic distribution of HVSs with 3-D velocities pointing back to the GC, assuming the initial binary stars are injected into the SMBH loss cone isotropically from a spherical nuclear star cluster. If the binaries are injected from a stellar disk, then this should be reflected accordingly in the final velocity distribution of observed hypervelocity stars (Zhang et al. 2013).

The Hills mechanism assumes an isolated SMBH, but it remains possible that an IMBH is also present in the GC and orbits Sgr A*. Yu & Tremaine (2003) constrained the allowed orbital properties of such an hypothesized IMBH (see also Gualandris & Merritt 2009). Interestingly, if an IMBH exists, this opens up another channel for producing HVSs. Specifically, if single stars pass close to the SMBH-IMBH pair, they can be flung out of the Galaxy at roughly the orbital speed of the IMBH (i.e., up to thousands of km s$^{-1}$), draining orbital energy from the BH binary.

This second mechanism for producing HVSs also predicts HVSs with 3-D velocities that point back to the GC. But, assuming isotropic injection of single stars into the SMBH-IMBH loss cone, the predicted velocity distribution should be skewed such that it is preferentially aligned with the orbital plane of the SMBH-IMBH binary. As shown in this paper using sophisticated 3-body integrations, the characteristic final ejection velocities associated with this mechanism should be lower than predicted by the standard Hills mechanism. Note, however, that while we compute the ejected velocities at fixed binary separations, to compute the overall expected distribution the IMBH orbit has to be self-consistently evolved (Marchetti et al. 2018a; Darbha et al. 2018). Moreover, an inspiralling IMBH will also disrupt the cusp of stars bound to Sgr A*, a process that can lead to a burst of stellar ejections at very high velocities (Sesana et al. 2008), which we don’t include in our model.

Finally, this is the only mechanism that can generate HVS binaries (Lu et al. 2007; Sesana et al. 2009; Wang et al. 2018), offering a potential means of constraining the possible presence of an IMBH in the Galactic Center.

2.2. Globular clusters

In Galactic globular clusters, the same mechanisms for producing HVSs in the GC could also be operating, provided IMBHs are present. The Hills mechanism could operate, if binary stars drift within the loss cone of any existing IMBHs (Fragione & Gualandris 2018a). As found in Leigh et al. (2014), if stellar-mass BHs are also present in globular clusters hosting IMBHs, then the most massive BH remaining in the system will quickly end up bound to the IMBH in a roughly Keplerian orbit but with a very high orbital eccentricity. This IMBH-BH binary could then produce HVSs by interacting directly with single stars in the cores of globular clusters, in close analogy with the production of HVSs by an SMBH-IMBH binary in the GC.

Ejection of HVSs from globular clusters predicts a mean HVS velocity that is much smaller than predicted for HVSs with a GC origin, due to the much smaller masses of IMBHs compared to SMBHs. It also predicts HVS velocities distributed roughly isotropically on the sky and pointing inward toward the central parts of the Galaxy and its disc, provided every globular cluster in the Galaxy contributes commensurably to HVS production (and assuming an isotropic distribution of globular clusters in the MW halo).

Ejections from this environment also predict the widest distribution of HVS velocities, since MW globular clusters have orbital velocities of order $\sim 200 \text{ km s}^{-1}$ but
with a wide range of orbital motions through the Galaxy. Hence, the predicted distribution of HVS velocities must be broadened accordingly by the mean globular cluster orbital velocity.

2.3. The Large Magellanic Clouds

Whether or not the Large Magellanic Clouds (LMC) are home to one or more massive BHs is an actively debated topic (Boubert & Evans 2016; Boubert et al. 2017). But, if the LMC is home to any massive BHs, then we might expect HVSs produced analogously to those discussed above, only with 3-D velocities pointing back to the LMC instead of the Milky Way. As mentioned before, two such candidate HVSs have been identified (Erkal et al. 2018; Hattori et al. 2018).

The orbital velocity of the LMC about the MW is of order \( \sim 300 \) km s\(^{-1}\) (Kallivayalil et al. 2013). Hence, this mechanism for HVS production also predicts a mean HVS velocity shifted to higher velocities by of order \( \sim 300 \) km s\(^{-1}\) relative to the Galactic rest frame. Note that this distribution is simply shifted to higher velocities, and does not suffer from the same broadening described above for HVSs produced from Galactic globular clusters. Thus, we might naively expect a comparable maximum velocity for both the globular cluster and LMC ejection scenarios, but a much broader velocity distribution for the former mechanism.

Interestingly, if there is an IMBH/SMBH in the LMC and it has a close binary BH companion, then (after correcting for the orbital motion of the LMC relative to the Milky Way, and the MW’s gravitational influence on the distribution of ejection velocities) the resulting distribution of HVSs may either resemble a torus for circular orbits (i.e., ejected preferentially in the orbital plane of the binary but with some dispersion) or a one-sided jet for eccentric orbits (e.g. Quinlan 1996; Sesana et al. 2006). If, on the other hand, an IMBH/SMBH is present in the LMC but has no binary companion, then the expected distribution of HVSs should be isotropic relative to the position of the IMBH/SMBH in the LMC.

2.4. Kicks during supernovae explosions in binaries

HVSs can also be produced in binary star systems when one of the companions explodes as a supernova (SN), ablatting the stellar progenitor completely. This blast wave should quickly flow beyond the original orbit of the companion, such that it is escapes to infinity with a final velocity of order the Keperian velocity at the time of explosion (in the direction of motion the exploding WD). However, in order for large velocities of order \( \gtrsim 1000 \) km s\(^{-1}\) to be achieved, both binary companions must be compact objects prior to the supernova explosion. Hence, most of the HVSs are expected to be white dwarfs (WDs) originating from compact accreting WD-WD binaries (Shen et al. 2018).

This mechanism predicts HVSs with 3-D velocities originating from the disk of our Galaxy, since this is where the majority of the progenitor WD-WD binaries are expected to reside. Most of these should be born from more massive stars with shorter lifetimes and hence associated with young star-forming regions, since the most massive WDs are needed in order to accrete enough material from their binary companions to exceed the Chandrasekhar limit. Recently, three candidate HVS WDs were identified by Shen et al. (2018) using GAIA data, which the authors postulate to have formed from kicks during SN explosions in WD-WD binaries.

### 3. SCATTERING EXPERIMENTS: METHOD

To calculate the ejected star velocities we use scattering experiments analyzed using the method originally presented in Quinlan (1996) and later built upon by Sesana et al. (2006) and Rasskazov & Merritt (2017). We assume every star is initially unbound from the SMBH-IMBH binary and approaches it from infinity. Then we follow its interaction with the binary until the star reaches the local escape speed, defined such that the star has positive total energy at spatial infinity. At the beginning of every simulation, we specify the following:

1. Binary mass ratio \( q \).
2. Binary eccentricity \( e \).
3. Initial stellar velocity (at infinity) \( v \).
4. Stellar impact parameter \( p \).
5. Two angles defining the initial orbital plane of the star \( \{\theta, \phi\} \).
6. One angle defining the direction of the initial stellar velocity with respect to its orbital plane \( \psi_b \).

The stellar orbit integrations are carried out using ARCHAIN, an implementation of algorithmic regularization developed specifically to treat small-N systems (Mikkola & Merritt 2008). The incoming star is considered mass-less which further simplifies the problem: the binary’s center of mass is always at the center of the coordinate system.

To speed up the computations, the stellar orbit is treated as Keplerian whenever the star is farther than 50 binary semimajor axes from the center of mass; whenever it leaves that sphere, we 1) calculate its coordinates and the time at which it re-enters the sphere, 2) calculate the binary phase at that time, and then 3) restart the 3-body integration with the new initial conditions. The reduction in the required CPU time can reach an order of magnitude for the runs with \( q \ll 1 \) when a significant fraction of the stars get captured on to very loosely
bound orbits (semimajor axes > 100) and perform hundreds of revolutions before finally being ejected. We confirm that this approximation does not introduce any noticeable bias into the distribution of HVS parameters.

During a simulation, we use the binary semimajor axis \( a \) as the unit of distance and the orbital velocity \( v_0 = \sqrt{GM/a} \) (where \( M = M_1 + M_2 \) is the total binary mass) as the unit of velocity, with the binary period being set equal to \( 2\pi \). For this reason, our simulation results do not depend on the binary mass and semimajor axis as long as \( p/a \) and \( v/v_0 \) are fixed.

It has been previously shown that a binary only becomes efficient at ejecting stars at semimajor axes \( a < a_h = GM_2/(4\sigma^2) \). For that reason, following SHM06, for every pair of \( \{q, e\} \) we sample \( v \) in the range \( 3 \times 10^{-3} \sqrt{q/(1+q)} < v < 30 \sqrt{q/(1+q)} \) with 80 logarithmically sampled points. This allows us to sample a Maxwellian distribution (using rejection sampling) for a relevant range of binary hardness at any \( q \): \( a/a_h \sim 4(v/v_0)^2(1+q)/q \sim 10^{-5} \ldots 10^3 \). For every value of \( v \) we perform \( 5 \times 10^4 \) scattering simulations, where \( \cos \theta \) and all the other angles are uniformly distributed, and \( p^2 \) is uniformly distributed in the range \([0, 25(1 + 0.4v^{-2})]\) which corresponds to a pericenter distance range \([0, 5]\). In this way, for every \( \{q, e\} \), we perform a total of \( 4 \times 10^6 \) simulations.

The simulations are stopped when one of the following conditions is met:

1. The star leaves the sphere of radius 50\(a\) with positive energy.
2. The total interaction timescale exceeds \(10^{10}\) yr (assuming parameters similar to the Milky Way \(M = 4 \times 10^6 M_\odot, \sigma = 70 \text{ km/s}\) and \(a = a_h\)).
3. The total time the star spends inside the sphere of radius 50\(a\) (when its orbit is not treated as Keplerian) exceeds \(10^4\) time units (1.6 \(\times\) 10^4 binary orbital periods).

Only in the first case the star is treated as ejected. Its velocity is calculated at infinity with its orbit being extrapolated from the radius 50\(a\) as Keplerian (hyperbolic). Stars falling into the latter two categories are discarded and not included in the simulated HVS dataset. Their fraction is usually the highest for the simulations with low \(v\), low \(q\) and high \(e\); for the fastest velocity bin it is always zero (the stars simply fly by). In the slowest velocity bin, 0.5%-3% and 6%-9% of all simulations fall into categories 2 and 3, respectively.

Given the scattering experiment data described above, it is possible to introduce the rotation of the stellar nucleus in the same way as in Rasskazov & Merritt (2017) or Gualandris et al. (2012):

1. Choose a direction for the stellar rotation axis.
2. Divide all the stars into “corotating” and “counter-rotating” depending on the sign of the projection of their initial angular momentum on to the axis of rotation.
3. Choose the fraction of corotating stars \(\eta \in [0, 1]\), and remove some stars accordingly.

### Table 2: Best-fit parameters for the hardening rate \(H\) (Eq. 3a)

| \(q\)   | \(\gamma\) | \(A\) | \(a_0/a_h\) |
|--------|------------|-------|-------------|
| \(q = 10^{-4}\), 0 | 11.1       | 2.72  | -0.83       |
| 0      | none       | 16.7  | -0.77       |
| \(q = 10^{-4}\), 0.9 | 12.5       | 2.03  | -0.74       |
| 0      | none       | 18.6  | -0.81       |
| \(q = 10^{-3}\), 0 | 22.2       | 3.77  | -0.80       |
| \(q = 10^{-3}\), 0.9 | 24.8       | 4.30  | -0.86       |

In what follows, we check the dependence of the hyper-velocity star parameters on \(\eta\) as well as on the mutual orientation of the binary and star orbital planes.

### 4. Scattering Experiments: Results

In this section we calculate various dimensionless parameters of the binary evolution necessary to model the distribution of HVS velocities. In accord with previous works, we define the hardening rate \(H\), mass ejection rate \(\dot{m}\) and the rate of eccentricity evolution \(J\) as

\[
H = \frac{\sigma d}{GM \ln((1/a)})
\]

\[
\dot{m} = \frac{dM_{ej}}{d \ln (1/a)}
\]

\[
K = \frac{d \ln (v/v_0)}{d \ln (1/a)}
\]

where \(M_{ej}\) is the stellar mass ejected by the binary. From the scattering experiment data, we calculate these parameters in the following way (see Appendix A for the derivation):

\[
H = 2\pi \frac{(1 + q)^2}{q} \left( \frac{p_{max}^2 v}{m_\odot} \right) \delta E_\ast \langle \delta L_{z,\ast} \rangle
\]

\[
J = \frac{\pi \sigma}{H} \left( \frac{p_{max}^2 v}{\delta E_\ast} \right)
\]

\[
K = \frac{1 - e^2}{2e} \left( \frac{\langle p_{max}^2 v \delta E_\ast \rangle - 1}{\langle p_{max}^2 v \delta E_\ast \rangle} \right)
\]

Here \(\langle \ldots \rangle\) means the average over all simulations (with Maxwellian velocity distribution with dispersion \(\sigma\)) and \(\langle \ldots \rangle_{ej}\) only includes the simulations where the final stellar velocity is above 5.5\(v\) (approximately the escape velocity from the MW center). \(p_{max}\) is the maximum value of the initial impact parameter (see Section 3) and \(m_\odot, v, \delta E_\ast, \delta L_{z,\ast}\) are the stellar mass, initial velocity and changes in energy and angular momentum, respectively. These equations also assume \(a = v_0 = 1\).

Fig. 1 (top) shows the values of \(H\) and \(J\) for different parameters of the binary. The values we got are in good agreement with Sesana et al. (2006). All random fluctuations are due to sampling of stars from the scattering experiments. We see that both of them are fairly independent of \(q\) and \(e\) and, following Sesana et al. (2006),
| $q$ value | $e$ value | Rotation | $A$ | $a_0/a_h$ | $\alpha$ | $\beta$ | $\gamma$ |
|----------|----------|----------|-----|--------|-------|------|-------|
| $10^{-4}$ | 0        | counter- | 0.278 | 0.262 | -0.233 | 2.281 | -0.625 |
| $10^{-4}$ | 0.9      | none     | 0.231 | 0.263 | -0.257 | 2.207 | -0.672 |
| $10^{-4}$ | 0.9      | counter- | 0.208 | 0.231 | -0.216 | 1.823 | -0.746 |
| $10^{-3}$ | 0        | none     | 0.483 | 0.169 | -0.121 | 0.937 | -1.523 |
| $10^{-3}$ | 0.9      | none     | 0.240 | 0.231 | -0.216 | 1.823 | -0.746 |
| $10^{-3}$ | 0.9      | counter- | 0.472 | 0.127 | -0.131 | 1.062 | -1.208 |

Fig. 1.— The dependence of the hardening and ejection rates on the binary hardness for a non-rotating stellar nucleus with different values of $q$ and $e$ (top) and $e = 0$ with different assumptions about the rotation of the host nuclear star cluster (bottom).
| $e$ rotation | $A$          | $a_0/a_h$ | $\gamma$ | $B$       |
|-------------|-------------|-----------|----------|-----------|
| $q = 1$     |             |           |          |           |
| 0.3 none    | $7.25 \times 10^{-2}$ | 0.614     | $-6.03$  | 0.000     |
| counter-    | 0.409       | $3.72 \times 10^{-2}$ | $-0.432$ | 0.542     |
| 0.6 none    | 0.132       | $7.08 \times 10^{-2}$ | $-0.958$ | 0.034     |
| co-         |             |           |          |           |
| $q = 0.1$   |             |           |          |           |
| 0.3 none    | 0.148       | 0.141     | $-0.703$ | $-0.003$  |
| counter-    | 1.487       | $4.02 \times 10^{-2}$ | $-0.150$ | 0.051     |
| 0.6 none    | 0.447       | $3.37 \times 10^{-2}$ | $-0.175$ | $-0.176$  |
| co-         | 0.246       | $4.01 \times 10^{-3}$ | $2.03 \times 10^{-2}$ | $-0.762$  |
| 0.9 none    | 0.147       | 0.222     | $-0.861$ | 0.005     |
| $q = 10^{-2}$|             |           |          |           |
| 0.3 none    | 0.263       | 1.33      | $-2.31$  | $-0.024$  |
| counter-    | $7.25$      | $8.21 \times 10^{-3}$ | $-0.012$ | $-4.84$   |
| 0.6 none    | 0.209       | 0.297     | $-1.30$  | $-0.014$  |
| co-         | 0.422       | 71.9      | $-1.45$  | $-1.45$   |
| 0.9 none    | 0.200       | 0.105     | $-0.371$ | $-0.092$  |
| $q = 10^{-3}$|             |           |          |           |
| 0.3 none    | 0.287       | $3.60 \times 10^{-3}$ | $-0.262$ | $-0.003$  |
| counter-    | $9.09$      | $6.37 \times 10^{-4}$ | $-0.015$ | $-8.14$   |
| 0.6 none    | 0.501       | $1.04 \times 10^{-2}$ | $-0.653$ | $-0.074$  |
| co-         | 0.944       | $1.41 \times 10^{-3}$ | $-0.0035$ | $-9.87$   |
| 0.9 none    | 0.233       | 10.3      | $-1.58$  | $-0.097$  |
| $q = 10^{-4}$|             |           |          |           |
| 0.3 none    | $-3.511$    | $2.11 \times 10^{-3}$ | $-0.0405$ | 3.90      |
| counter-    | $-0.928$    | 86.2      | $-7.63$  | 0.170     |
| 0.6 none    | 0          | $-0.565$  | $-0.474$ |
| co-         | 0          | $-0.565$  | $-0.474$ |
| 0.9 none    | $-2.145$    | 122       | $-3.06$  | 1.69      |
| $q = 10^{-5}$|             |           |          |           |
| 0.3 none    | $-3.511$    | $2.11 \times 10^{-3}$ | $-0.0405$ | 3.90      |
| counter-    | $-0.928$    | 86.2      | $-7.63$  | 0.170     |
| 0.6 none    | 0          | $-0.565$  | $-0.474$ |
| co-         | 0          | $-0.565$  | $-0.474$ |
| 0.9 none    | $-2.145$    | 122       | $-3.06$  | 1.69      |
Fig. 2.— The dependence of the rate of eccentricity evolution on the binary hardness for a non-rotating stellar nucleus with different values of $q$ and $e$. 
can be analytically approximated as

\[ H = A(1 + a/a_0)^\gamma, \]
\[ J = A(a/a_0)^\alpha(1 + (a/a_0)^\beta)^\gamma. \]  

The parameter values for these approximations are listed in Tables 2 and 3. We also consider both completely corotating/counterrotating stellar nuclei (Fig. 1, bottom). \( H \) is \( \sim 2 \) times higher in the corotating case compared to the counterrotating one, and this difference persists for all values of \( a/a_h \) (Fig. 1, bottom left).\(^2\) As for the dependence of \( J \) on rotation, it is more complex: \( J_{\text{corot}} \approx 0.5J_{\text{counterrot}} \) for \( a/a_h \leq 0.3 \) and \( J_{\text{corot}} \approx 2J_{\text{counterrot}} \) for \( a/a_h \geq 0.3 \) (Fig. 1, bottom right). We have also performed calculations to emulate a co-/counter-rotating stellar disk by only considering stars with \( \theta < \pi/20 \) and \( \theta > 19\pi/20 \), respectively. In this case, the difference in co- and counter-rotating \( H \) and \( J \) is more pronounced: a factor of 3-5 instead of 2.

\(^2\) This is in contrast to the equal-mass binary case studied in Rasskazov & Merritt (2017) where \( H_{\text{corot}} = H_{\text{counterrot}} \) for \( a \ll a_h \) and \( H_{\text{corot}} \approx -H_{\text{counterrot}} < 0 \) for \( a \gg a_h \).

Fig. 2 shows the values of \( K \) for different parameters of the binary. Unfortunately, at \( q < 0.01 \) it becomes hard to determine the exact value of \( K \) as the contribution from random noise increases. As in Sesana et al. (2006), we use the following analytical approximation for \( K(a/a_h) \) with parameters listed in Table 4:

\[ K = A(1 + a/a_0)^\gamma + B. \]  

Even though they agree with Quinlan (1996), our values of \( K \) differ significantly from those of Sesana et al. (2006): they are systematically higher by up to a factor of 1.5. It turns out, there is a mistake in Sesana et al.’s procedure for the calculation of \( K \): they calculate \( K \) for a single-velocity stellar distribution (Sesana et al. 2006, Eq. 12) and then average it over the Maxwellian distribution—the correct way is instead to separately velocity-average the numerator (\( d\sigma/\mu \)) and the denominator (\( d\ln a/\mu \)) in the definition for \( K \). For this reason, we also cite in Table 4 the \( K \) values for mass ratios \( q > 10^{-2} \) which are ruled out for the case of an IMBH in our galactic center (Merritt 2013).

Curiously, somewhere between \( q = 10^{-4} \) and \( q = 10^{-3} \) (the regime unexplored in any previous work) \( K \) for non-rotating case switches from mostly positive to mostly negative, at least for \( e = 0.6 - 0.9 \). The reasons for that are unclear but that implies we shouldn’t expect the orbit of a low-mass IMBH \( (\lesssim 10^3 M_\odot) \) to be eccentric.

Fig. 3 shows \( K \) for co- and counterrotating stellar environments. For \( q \lesssim 10^{-2} \), we have confirmed the previous findings that the binary eccentricity tends to decrease in a corotating environment and increase in a counterrotating environment (Sesana et al. 2011; Rasskazov & Merritt 2017), \( |K| \) being about an order of magnitude larger compared to the nonrotating case and weakly dependent on \( a/a_h \) (Fig. 3, top). However, for \( q \lesssim 10^{-3} \) the rotation seems to be much less significant although it’s hard to tell because of large numerical errors (Fig. 3, bottom). An equal-mass corotating binary presents a special case as \( K \) becomes infinite at \( a/a_h \approx 10 \); it can be fitted as

\[ K = -26.6 (10 - a/a_h)^{-1.77}. \]  

This happens because \( H \) becomes negative for sufficiently soft equal-mass binaries, as was discovered in Rasskazov & Merritt (2017).

Fig. 4 (top and middle) shows the distribution of ejected stars’ velocities for various binary parameters. These are in good agreement with Sesana et al. (2006).\(^3\) The maximum is due to the initial (Maxwellian) velocity distribution having a peak at \( \sim \sigma = \frac{1}{2} \sqrt{\frac{a}{a_0} + \frac{a_0}{a}} \). The component of this distribution which is relevant to the HVS problem is the high-velocity tail \( v > v_{\text{min}} \).

\[ v_{\text{min}} = v_0 \sqrt{\frac{2q}{1 + q}} = 2\sqrt{\frac{a_0}{a}} \sqrt{\frac{a_h}{a}} \sim 280 \text{ km/s}. \]  

In this hypervelocity tail \( \frac{dN}{d\log v} \sim v^\alpha \), \( \alpha \approx -3 \) irregardless of the binary parameters, including the absolute number of stars in the tail ejected per unit time is

\(^3\) Note that the plots in the current paper show \( \frac{dN}{d\log v} = \frac{vdN}{dv} \).
Fig. 4.— Top and middle: the distribution of ejection velocities (in units of the binary orbital velocity $v_0 = \sqrt{\frac{GM}{a}}$) for different parameters of the binary. Bottom: distribution of the direction angles of the stellar escape velocity, where $\theta = 0$ is the direction of the massive BH binary angular momentum and $\phi = 0$ is the direction of the SBH orbital pericenter. All distributions are normalized such that the total number is equal to 1.
where here and the following we set $D$ conservation. If a binary star starts from an initial distance $r$ when a numerical value is needed. The distance of closest approach can be computed using angular momentum when a numerical value is needed. The distance of closest approach is determined by (Merritt 2002). All distributions are normalized to unit area.

The bottom row of Fig. 4 shows the distribution of HVS velocity directions. All the ejected stars are distributed almost spherically ($\sin \theta$ and uniformly in $\phi$) as most stars interact with the binary very weakly. However, if we only consider the stars fast enough to escape from the GC (taking the escape velocity above \( \sim 6\sigma \)), they are preferentially ejected in the direction of the massive BH binary orbital plane, as was also found in Sesana et al. (2006). The distribution of $\phi$ for these fast stars is also not uniform, with a maximum around $\sim 3\pi/4$. Azimuthal anisotropy has also been observed by Sesana et al. (2006), although they found that the HVSs are preferentially ejected in the direction of the secondary BH velocity at pericenter ($3\pi/2$); the reasons for this discrepancy remain unclear, but we return to this interesting discrepancy in Section 6.

5. Hills Mechanism

In this section, we briefly summarize the standard Hills mechanism and the SMBH-IMBH scenario. A binary of total mass $m_b$ and semi-major axis $a_0$ is tidally disrupted whenever it approaches a single SMBH of mass $M_{\text{SMBH}}$ within a distance of order the binary star tidal radius

\[
r_t \approx 10 \text{ AU} \left( \frac{a_0}{0.1\text{AU}} \right) \left( \frac{M_{\text{SMBH}}}{m_b/4M_\odot} \right)^{1/3}, \tag{7}
\]

where here and the following we set $M_{\text{SMBH}} = 4 \times 10^6 M_\odot$ when a numerical value is needed. The distance of closest approach can be computed using angular momentum conservation. If a binary star starts from an initial distance $D$ with transverse speed $v$, the distance of closest approach $r_{\text{min}}$ will be

\[
v D = \left( \frac{G M_{\text{SMBH}}}{r_{\text{min}}^2} \right)^{1/2} r_{\text{min}}. \tag{8}
\]

In the case $r_{\text{min}} \lesssim r_t$, the binary star is tidally separated and the former companion is dissociated. There are three possible outcomes for the tidal breakup of a binary: (i) production of an HVS and an S-star, (ii) production of 2 S-stars, (iii) capture of the whole binary. From energy conservation, these two latter can occur only for binaries whose center of mass is on a bound--parabolic--orbit, while the former case the approaching binary should be close to a parabolic trajectory. In the case of a triple (Fragione & Gualandris 2018b) or quadruple star (Fragione 2018), even more outcomes are possible.

For a binary centre of mass approaching on a nearly parabolic orbit, the ejected star has a velocity at infinity with respect to the black hole of (Hills 1988; Bromley et al. 2006; Sari et al. 2010; Kobayashi et al. 2012)

\[
v_{\text{ej}} = K_g \sqrt{\frac{2 G m_c}{a_0}} \left( \frac{M_{\text{SMBH}}}{m_b} \right)^{1/6} \approx 1500 \frac{\text{km}}{s} \sqrt{\frac{m_c}{\text{0.1AU}}} \left( \frac{M_{\text{SMBH}}}{m_b/2M_\odot} \right)^{1/6}, \tag{9}
\]

where $m_c$ is the mass of companion star, that remained bound to the SMBH and $K_g$ is a numerical coefficient of order unity that only depends on the specific geometry of the encounter (e.g., binary phase and binary pericenter, see figure 10 in Sari et al. (2010)). For a given binary, Bromley et al. (2006) and Fragione & Gualandris (2018a) numerically showed that the overall distribution is well approximated by a Gaussian distribution with mean $v_{\text{ej}}$ and dispersion $\sigma \sim 0.2-0.3$ $v_{\text{ej}}$. The broadening of the distribution around the Hills peak $v_{\text{ej}}$ is due to averaging over the random orientations of the initial binary phases, orientations and eccentricities. We also remark that for a parabolic orbit the ejection probability is exactly 50% for the primary, while the primary gets preferentially captured (ejected) for elliptical (hyperbolic) approaching trajectories (Sari et al. 2010; Kobayashi et al. 2012). The velocity distribution for a population of binary with mass and semimajor axis distributions can then be analytically and accurately using Eq. (9) with $K_g = 1$ (Rossi et al. 2014).

To compare the expected ejection velocity distribution obtained in the SMBH-IMBH case to the Hills mechanism case, we run 1 million 3-body simulations of the close encounter of a binary star and an SMBH. Also in this case, we use the ARCHAIN algorithm to accurately integrate the motions of our systems (Mikkola & Merritt 2008). We set the initial conditions of our 3-body simulations following the prescriptions of Ginsburg & Loeb (2006, 2007) and Fragione & Gualandris (2018b). We consider equal-mass binaries, and sample the initial distribution of semi-major axes ($a_0$) from a uniform or log-uniform distribution, in the range 0.01 AU-1 AU (Fra-
We also assume a thermal distribution of binary eccentricities \( e_b \), and check that the sampled binaries satisfy \( a_b (1 - e_b) > R_\star \) \((R_\star \text{ is the stellar radius)}\). We then randomly sample the pericenter distance \( r_p \) of the binary according to a probability \( \propto r_p \), in the range \( 0 - 2R_b \), where \( R_b = r_b(a_b = 1 \text{ AU}) \), i.e. twice the maximum tidal radius of the softest binary in our semi-major axis distribution. We note that this choice for the distribution of \( r_p \) implies that wider binaries are preferentially separated because their tidal radius \( r_t \propto a_b \) is larger, enhancing lower velocity ejections (see eq.9). We note, however, that this is not the only possible way to distribute \( r_p \), as binaries that diffuse in angular momentum space by two-body encounters would be instead mostly separated at \( r_p \sim r_t \), implying a disruption probability independent of \( a_b \).\footnote{Factually, we are assuming that the refilling of the loss cone with binary orbits occurs in the “full” regime (Lightman & Shapiro 1977; Rossi et al. 2014).} Given \( a_b \) and \( e_b \) of a specific sampled binary, we integrate the 3-body system if \( r_p < 2r_b \), otherwise we reject the binary.

Figure 5 shows a comparison between the expected ejection spectrum of the Hills mechanism and the SMBH-IMBH scenario. In the Hills (1988) case, we consider both stars to have masses \( m_1 = m_2 = 1 \text{ M}_\odot \). In the SBM-IMBH scenario, we take \( q = 10^{-4} - 10^{-3} \) and \( a/a_h = 0.1-1 \), within the allowed parameter space of the putative IMBH in the GC (Merritt 2002). In the case \( a/a_b = 1 \), the SBM-IMBH scenario predicts much smaller final velocities, with a distribution peaked at \( \sim 200 \text{ km s}^{-1} \), while the Hills scenario typically produces higher velocities peaked at \( \sim 800 \text{ km s}^{-1} \). However, for a smaller SBM-IMBH semi-major axis \( a/a_b = 0.1 \) and stellar velocities \( v \gtrsim 500 \text{ km s}^{-1} \) (about the minimum velocity for a star to become a HVS, Sesana et al. 2006), the SBM-IMBH scenario distribution looks similar to the Hills scenario.

In the Hills scenario, we note that we do not find significant differences between adopting a log-uniform and uniform distribution in the binary semi-major axis. We have also run models with \( m_1 = m_2 = 3 \text{ M}_\odot \). Also in this case, we do not find any significant difference with the case \( m_1 = m_2 = 1 \text{ M}_\odot \). This is because, while a larger mass implies typically a larger ejection velocity (Eq. 9), the sampled initial binary semi-major axes are typically larger (to satisfy \( a_b (1 - e_b) > R_\star \)).

6. CONCLUSIONS

We have performed a series of 3-body scattering experiments of an initially unbound star getting ejected by a potential SMBH-IMBH binary in our galactic center. The IMBH mass was assumed to be in the range \( q = 10^{-4} - 10^{-2} \) of the SMBH mass. The new features compared to previous papers are 1) scattering experiments for \( q \leq 10^{-3} \) and 2) using the ARCHAIN numerical code for the scattering experiments.

We found the distribution of HVS velocities to be a power-law \( (dN/dv) \propto v^{-4} \), regardless of the binary or stellar parameters. The HVS velocity directions are concentrated around the binary orbital plane and, in the case of an eccentric binary, they have a preferred direction in the binary plane. We have also calculated the stellar ejection rate \( J \) as well as the evolution rates of the binary semimajor axis \( H \) and eccentricity \( K \). We found \( J \) and \( H \) to be fairly independent of \( q \). \( K \), however, changes at the lowest values of \( q \) we have probed \((10^{-4} - 10^{-3})\), becoming negative at most values of \( a \) and \( e \). Therefore, we should probably expect the IMBH orbit to be circular. This result is unexpected and deserves further investigation as \( K \) shows quite a consistent behavior at \( q = 1 - 10^{-3} \). Adding rotation of the stellar nucleus does not affect that conclusion (see below).

We found two discrepancies with the results of Sesana et al. (2006). First, our values of \( K \) are up to 1.5 times higher due to Sesana et al. (2006) using an incorrect procedure to calculate \( K \). Also, our simulations show a different distribution for \( \phi \) – the direction of the ejection velocity in the plane of the binary – which is non-uniform for eccentric binaries. Its peak is not at \( 3\pi/2 \) as in Sesana et al. (2006) (the direction of the IMBH velocity at its pericenter) but rather at \( \lesssim \pi \). We could not determine the source for this discrepancy. However, the difference would be hard to test observationally unless we have independent constraints on the IMBH pericenter (and Sesana et al. (2006) do not provide the exact distribution of \( \phi \) in their paper).

Another new result of this paper is simulations of a corotating/counterrotating stellar nucleus where only the stars with positive/negative \( L_z \) were selected. We find the following:

- Corotation/counterrotation decreases/increases the hardening rate by \( \sim 50\% \).
- Corotation decreases/increases the stellar ejection rate for binary semimajor axes below/above \( \sim 0.5 a_h \) (the opposite for counterrotation).
- For \( q \gtrsim 10^{-2} \), eccentricity tends to decrease/increase in corotating/counterrotating systems, and the absolute value of \( K \) is much higher compared to the nonrotating case. For \( q \lesssim 10^{-3} \), however, \( K \) is weakly dependent on rotation.

Finally, we have also compared the SBM-IMBH ejection scenario to the standard Hills mechanism. We find that the Hills mechanism ejects stars at higher velocities compared to the SBM-IMBH mechanism for the parameters explored in this paper (see Figure 5). However, there are enough unknown parameters that do not allow us to make this a general statement. On one hand, we showed that for small SBM-IMBH separation \( a/a_b \leq 0.1 \) the high velocity tail becomes harder and similar to that from the Hills mechanism. On the other, the high velocity tail in the Hills mechanism crucially depends on the assumed star binary mass-ratio and separation distributions, that we are not widely exploring here. In particular, softer high velocity tails can be obtained with star binary distributions consistent with current observations (Rossi et al. 2017).

These results will be used in our next paper to construct samples of ejected stars, where we will take into account the moment of ejection, orbit in the Milky Way potential and also the SBM-IMBH binary evolution for the case of IMBH slingshot ejections. These samples will then be compared to the observed HVS distributions (using mixture models to combine all of the HVS production...
scenarios described in this paper) to test the hypothesis that they might have been generated by one of the two mechanisms we consider.

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APPENDIX

A. CALCULATION OF $H, J$ AND $K$

By definition,

$$H = -\frac{\sigma}{G\rho a^2} \frac{da}{dt} = -\frac{2\sigma}{(GM)^2} \frac{dE}{dt}$$  \hspace{1cm} (A1)

where $E$ is the binary orbital energy. Assuming an infinite uniform distribution of stars$^6$ (cf. Merritt 2002, Eq. 16a),

$$\frac{dE}{dt} = \int_{0}^{\infty} dv \int_{0}^{p_{\max}(v)} 2\pi p \, dp \, vnf(v) \langle \delta E \rangle_{\theta,\phi} = -\int_{0}^{\infty} dv \int_{0}^{p_{\max}(v)} 2\pi p \, dp \, vnf(v) \langle \delta E^* \rangle_{\theta,\phi}$$  \hspace{1cm} (A2)

where $\delta E$ and $\delta E^*$ are changes in the binary energy and stellar energy, respectively, for a single scattering event, $f(v)$ and $n$ are respectively the initial stellar velocity distribution and number density, and $\langle \ldots \rangle$ means averaging over all angles. To calculate this integral numerically from our simulations, we use a Monte-Carlo method:

$$\int F(x) \, dx = \langle F \rangle \int dx$$  \hspace{1cm} (A3)

where $F$ is some function and $\langle F \rangle$ is its average value over the integration region. Given a set of simulations with an uniform distribution of $p^2$ and a Maxwellian velocity distribution, and also the fact that $\rho = m_* n$, it is straightforward to derive Eq. (2a).

Similarly,

$$J = \frac{1}{M} \frac{dM_{ej}}{dt} = \frac{1}{a} \frac{\sigma}{HGM\rho} \frac{dM_{ej}}{dt},$$  \hspace{1cm} (A4a)

$$\frac{dM_{ej}}{dt} = m_* \int_{0}^{p_{\max}(v)} dv \int_{0}^{p_{\max}(v)} 2\pi p \, dp \, vnf(v)$$  \hspace{1cm} (A4b)

and

$$K = \frac{de}{dt} \left( \frac{da}{dt} \right)^{-1} a = \frac{1 - e^2}{e} m_* \left( \frac{M}{\mu L_2} \frac{dL_{z,*}}{dt} - a \frac{dE_*}{dt} \right) \left( -\frac{2a^2 m_*}{GM\mu} \right)^{-1} a$$  \hspace{1cm} (A5a)

$$\mu \equiv \frac{M_1 M_2}{M_1 + M_2}.$$  \hspace{1cm} (A5b)

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