Abstract: We have prepared $\text{Ca}_{1-x}\text{K}_x\text{WO}_4_{1-x/2}$ solid solutions with the Scheelite-type structure to investigate high-temperature electrochemical properties. Room-temperature X-ray diffraction suggested the solid solution range was $x \leq 0.2$, since the second phase presumably of $\text{K}_2\text{WO}_4$ was detected for $x = 0.3$. For all the substituted samples up to $x = 0.4$, a large jump in conductivity has been observed around 500 $^\circ$C. At higher temperatures, oxide ion conduction is found to be predominant even for $x = 0.4$, exceeding the solution limit estimated from the room-temperature XRD. The conductivity at high temperature is essentially proportional to the amount of substituted potassium ions up to $x = 0.4$, indicating that oxide ion conduction is associated with the formed oxide ion vacancy. High-temperature X-ray diffraction detected no apparent change in lattice parameters around 500 $^\circ$C for $x = 0.1$, and the remaining second phase seems to be incorporated into the Scheelite lattice at high temperatures.

Keywords: $\text{CaWO}_4$; oxide ion conductor; oxide ion vacancy; high-temperature XRD

1. Introduction

Considerable attention has been focused upon the oxide ion conductors for the application of the electrolyte of SOFC (Solid Oxide Fuel Cell) [1–3]. Since the major electrolyte materials of SOFC, such as stabilized zirconia or doped ceria, belong to the Fluorite-type structure; Scheelite-type structured materials derived from the Fluorite-type are a potential candidate for the oxide ion conductors [4]. We have intensively studied the $\text{PbWO}_4$-based oxide ion conductors with the Scheelite-type structure [5–8]. When lanthanum ions are partly substituted into the lead site of $\text{PbWO}_4$, forming oxide ion interstitials such as $\text{Pb}_{1-x}\text{La}_x\text{WO}_4_{x/2}$, high oxide ion conduction appears at elevated temperatures. Such a defect structure has been confirmed by the powder density measurements [6]. On the other hand, $\text{CaWO}_4$ with the mineral name of “Scheelite” is unlikely to form a solid solution by lanthanum substitution to create oxide ion interstitials. Nevertheless, in recent years, we have found that Cs-substituted $\text{CaWO}_4$ with the form $\text{Ca}_{1-x}\text{Cs}_x\text{WO}_4_{x/2}$ exhibits oxide ion conduction at elevated temperatures [9]. Since most oxide ion conductors with the Fluorite-type employ oxide ion vacancy for the oxide ion diffusion, mono-valent ion substitution for $\text{CaWO}_4$ would be a promising strategy for...
exploring the new type of oxide ion conductors. Considering that the ionic radius of the K⁺ ion (165 pm for 8-coordinate) is closer to that of Ca²⁺ (126 pm) rather than Cs⁺ (188 pm) [10], potassium substitution is more appropriate for the solid solution formation with CaWO₄. In the present study, we prepared the solid solution of Ca₁₋ₓKₓWO₄₋ₓ/2 to investigate the high-temperature electrochemical properties, and thereafter, high-temperature X-ray diffraction experiments were carried out emphasizing the phase transition phenomena.

2. Materials and Methods

Ca₁₋ₓKₓWO₄₋ₓ/2 samples were prepared by conventional solid-state reaction method, and were started using CaCO₃, H₂WO₄, and K₂CO₃. The calcining and sintering temperatures were selected as 800 and 1000 °C, respectively, as per the previous Cs-substituted system [9]. The obtained samples were analyzed by X-ray diffraction with CuKα radiation (XRD-6000; Shimadzu, Kyoto, Japan). Conductivity measurements were carried out by means of two-probe AC method, and oxygen gas concentration cells were constructed using the sample discs as electrolytes to evaluate the charge carrier. Pt electrodes were used for electrochemical measurements. In the present study, TG-DTA (DTG-50; Shimadzu, Kyoto, Japan) experiments up to 1000 °C have also been carried out to investigate the phase transition of the sample.

High-temperature X-ray diffraction experiments (AXS D8 Discover; Bruker, Billerica, MA, USA) up to 700 °C were then carried out for x = 0.1 and 0.4 to investigate the structural variation with temperature. The diffracted X-ray was collected by a 2D-detector in the diffractometer for 180 s per measurement. Lattice parameters were refined by the Rietveld method using RIETAN code [11] assuming the Scheelite-type structure with the space group of I4₁/a.

3. Results and Discussion

We first carried out the preliminary experiments to check the solid solubility and electric conductivity for various alkaline ion substituted CaWO₄s with the form Ca₁₋ₓAₓWO₄₋ₓ/2 (A: alkaline ion). From the room-temperature X-ray diffraction experiments, the solid solution limits were determined as x = 0.15, 0.10, 0.20 for Cs⁺, Rb⁺, and K-substitutions, respectively. As for Na-substitution, the solid solution cannot be obtained even for x = 0.05. We thus compared the high-temperature electric conductivities in these three compounds substituted by Cs⁺, Rb⁺ and K⁺ ions fixing the concentration as x = 0.1. Figure 1 compares the Arrhenius plots of conductivity for various alkaline ion substituted samples of Ca₁₋ₓAₓWO₄₋ₓ/2 (x = 0.1). While the Cs-substituted system gradually decreases the conductivity with reducing temperatures, the Rb- or K-substituted systems keep the relatively higher conductivity down to the intermediate temperatures with a drop in conductivity around 600 or 500 °C. On the other hand, all the substituted systems possess the similar conductivities as well as the similar slopes above 900 °C. Namely, keeping the higher conductivity down to the intermediate temperature exhibits for the K-substituted system. Accordingly, we carried out the electrochemical and structural studies focusing on the K-substituted CaWO₄.

![Figure 1. Arrhenius plots of conductivity for Ca₀.₉₄A₀.₀₆WO₄. △: A = K, □: Rb, and ◇: Cs. Conductivity of the pristine CaWO₄ is also plotted by closed circles (●).](image-url)
Figure 2 shows the X-ray diffraction patterns of Ca\textsubscript{1−x}K\textsubscript{x}WO\textsubscript{4−x/2} measured at room temperature. While all the diffraction peaks can be assigned as the Scheelite-type structure for \( x \leq 0.2 \), some additional peaks presumably due to K\textsubscript{2}WO\textsubscript{4} (PDF: 21-1010) or K\textsubscript{4}WO\textsubscript{5} (PDF: 24-0904) are observed at \( x = 0.3 \). Therefore, the solid solution range is evaluated as \( x \leq 0.2 \) for Ca\textsubscript{1−x}K\textsubscript{x}WO\textsubscript{4−x/2}. The Arrhenius plots in conductivity measured for Ca\textsubscript{1−x}K\textsubscript{x}WO\textsubscript{4−x/2} (\( x = 0–0.4 \)) are represented in Figure 3a. As plotted for \( x = 0.1 \) in Figure 1, all the substituted samples exhibit the conductivity enhancement from CaWO\textsubscript{4} by more than three orders of magnitude. Moreover, a large jump in conductivity is also observed around 500 °C. It should be noted that, at the higher temperature region, conductivity enhancement continues even after exceeding the solubility limit of \( x = 0.2 \). We assumed that excess potassium ions are incorporated into the Scheelite lattice around 500 °C to form oxide ion vacancy as the nominal form of Ca\textsubscript{1−x}K\textsubscript{x}WO\textsubscript{4−x/2} showing a conductivity jump. DTA measurements were then carried out to investigate this phenomenon. The obtained DTA traces are represented in Figure 4. For \( x = 0.3 \) or 0.4, a small endothermic peak is observed around 500 °C in the heating direction, suggesting that formation of the solid solution would occur at this temperature. Moreover, even for \( x = 0.2 \), a very small peak is still detected at this temperature.

![Figure 2. X-ray diffraction patterns of Ca\textsubscript{1−x}K\textsubscript{x}WO\textsubscript{4−x/2} obtained at room temperature.](image)

![Figure 3. (a) Arrhenius plot of conductivity for Ca\textsubscript{1−x}K\textsubscript{x}WO\textsubscript{4−x/2}. \( x = 0 \), \( \triangle: 0.1 \), \( \square: 0.2 \), \( \triangledown: 0.3 \), and \( \triangledown: 0.4 \); (b) Conductivity isotherms of Ca\textsubscript{1−x}K\textsubscript{x}WO\textsubscript{4−x/2} at 400, 600, and 800 °C.](image)
To clarify the compositional dependence of the conductivity, the measured electric conductivity is plotted versus potassium concentration as in Figure 3b. At 400 °C, the EMFs (Electromotive Forces) are plotted in Figure 5a, where the calculated EMF, assuming Nernst equation, is:

\[
EMF = \frac{R \cdot T}{4F} \ln \frac{P_{\text{O}_2}(1 \text{ atm})}{P_{\text{N}_2}(0.21 \text{ atm})}
\]

and is indicated by the dashed line. Since the measured EMFs agree well with the calculated one, the predominant charge carrier is the oxide ions. In Figure 5a, the more interesting aspect is that EMFs obtained for the \(x = 0.3\) or \(0.4\) beyond the solution limit also coincide with the Nernstian value. To clarify the compositional dependence of the conductivity, the measured electric conductivity is plotted versus potassium concentration as in Figure 3b. At 400 °C, conductivity increases with the potassium composition up to \(x = 0.3\), followed by a drop at \(x = 0.4\). However, the linear relationship between conductivity and potassium concentration can be seen at 600 or 800 °C. Therefore, excess potassium ions are supposed to be incorporated into the Scheelite lattice to form oxide ion vacancy around 500 °C, which allows the high oxide ion diffusion.

![Figure 4](image-url)  
**Figure 4.** DTA traces of \(\text{Ca}_{1-x}\text{K}_x\text{WO}_4-x/2\). Red arrows indicate the small endothermic peak observed in the heating direction.

![Figure 5](image-url)  
**Figure 5.** (a) EMFs of the oxygen gas concentration cells as follows using \(\text{Ca}_{1-x}\text{K}_x\text{WO}_4-x/2\) sample discs as the electrolyte. Air (\(P\text{O}_2 = 0.21 \text{ atm}\)) | \(\text{Ca}_{1-x}\text{K}_x\text{WO}_4-x/2\) | \(\text{O}_2\) gas (\(P\text{O}_2 = 0.21 \text{ atm}\)). triangle: \(x = 0.1\), square: \(0.2\), circle: \(0.3\), and triangle: \(0.4\). Dashed line denotes the Nernstian value; (b) Discharge plot of the oxygen gas concentration cell employing \(\text{Ca}_{1-x}\text{K}_x\text{WO}_4-x/2\) (\(x = 0.1\)) measured at 1000 °C. The calculated line was assuming only the ohmic loss.
High-temperature X-ray diffraction experiments were then performed focusing upon the conductivity jump accompanied by the endothermic heat at 500 °C. Figure 6 shows the XRD patterns of Ca$_{1-x}$K$_x$WO$_{4-x/2}$ (x = 0.1) measured at various temperatures. While diffraction peaks shift toward a lower diffraction angle with temperature due to thermal expansion, any distinct change in peak was not observed around 500 °C. The lattice parameters obtained by the Rietveld refinements are plotted versus temperature in Figure 7. Both a- and c-length increase uniformly without any apparent discontinuity, suggesting that the conductivity jump observed around 500 °C is not accompanied by the drastic change in structure or apparent phase transition. On the other hand, for higher potassium introduction as x = 0.4, diffraction peaks of the second phase were detected at room temperature in Figure 8. Excess XRD peak at 2θ = 30.3° does not shift as other peaks associated with Scheelite-type structure, almost diminishing at 700 °C. This temperature is a little higher than that of the conductivity jump with the endothermic peak, which would be due to that undissolved potassium component, which remains even at the measurement of 700 °C. Assuming that the solution range becomes wider at higher temperatures, the residual second phase would dissolve into the Scheelite lattice above 500 °C to create oxide ion vacancies even for x = 0.4, which would directly contribute to the oxide ion conduction. Even though any excess diffraction peak was not detected for x = 0.2 at room temperature, dissolution of a very small amount of potassium ions into the Scheelite lattice might occur for the observed very small endothermic heat at 500 °C. In addition to the solid solution formation, subtle disordering of oxide ions should be considered, which would be made based on the neutron diffraction as a future work.

![Figure 6](image6.png)

Figure 6. X-ray diffraction patterns of Ca$_{1-x}$K$_x$WO$_{4-x/2}$ (x = 0.1) measured at high temperatures up to 700 °C.

![Figure 7](image7.png)

Figure 7. Temperature dependence of the lattice parameters of Ca$_{1-x}$K$_x$WO$_{4-x/2}$ (x = 0.1).
4. Conclusions

The solid solution range of Ca$_{1-x}$K$_x$WO$_4$−x/2 is estimated as x ≤ 0.2 from the room-temperature X-ray diffraction experiments, while a slight amount of endothermic heat in DTA trace was observed around 500 °C on heating for x = 0.2. Above this temperature, oxide ion conduction appears to enhance the conductivity by more than three orders of magnitude. High-temperature oxide ion conductivity increases linearly with the potassium substitution beyond the room-temperature solid solution limit to achieve 0.01 Scm$^{-1}$ at 600 °C for x = 0.4. High-temperature X-ray diffraction suggested any apparent structural change occurs for x = 0.1, while presumably K$_2$WO$_4$ of the second phase dissolves into the Scheelite lattice at 700 °C. K-substituted CaWO$_4$ shows higher conductivity in comparison with the Cs-substituted system at the intermediate temperature of 600 °C.

Author Contributions: S.T. conceived the investigation and wrote the manuscript. S.S. performed the most of electrochemical experiments and T.S. verified partly. H.K. collected the high-temperature XRD data. T.Yt, T.E. and T.Yo contributed to refine the discussion.

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