On the black hole content and initial mass function of 47 Tuc

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ABSTRACT
The globular cluster (GC) 47 Tuc has recently been proposed to host an intermediate-mass black hole (IMBH) or a population of stellar-mass black holes (BHs). To shed light on its dark content, we present an application of self-consistent multimass models with a varying mass function and content of stellar remnants, which we fit to various observational constraints. Our best-fitting model successfully matches the observables and correctly predicts the radial distribution of millisecond pulsars and their gravitational accelerations inferred from long-term observations. The data favours a population of BHs with a total mass of $430^{+386}_{-301}$ M$_\odot$, but the most likely model has very few BHs. Since our models do not include a central IMBH and accurately reproduce the observations, we conclude that there is currently no need to invoke the presence of an IMBH in 47 Tuc. The global present-day mass function inferred is significantly depleted in low-mass stars (power-law slope $\alpha = -0.52^{+0.17}_{-0.16}$). Given the orbit and predicted mass-loss history of this massive GC, the dearth of low-mass stars is difficult to explain with a standard initial mass function (IMF) followed by long-term preferential escape of low-mass stars driven by two-body relaxation, and instead suggests that 47 Tuc may have formed with a bottom-light IMF. We discuss alternative evolutionary origins for the flat mass function and ways to reconcile this with the low BH retention fraction. Finally, by capturing the effect of dark remnants, our method offers a new way to probe the IMF in a GC above the current main-sequence turn-off mass, for which we find a slope of $-2.49 \pm 0.08$.

Key words: galaxies: star clusters – globular clusters: general – globular clusters: individual: 47 Tuc – stars: kinematics and dynamics – stars: luminosity function, mass function – stars: black holes.

1 INTRODUCTION
Postulated to populate the mass regime between stellar-mass black holes (BHs) and supermassive black holes (SMBHs), intermediate-mass black holes (IMBHs; $\sim 10^2 - 10^5$ M$_\odot$) could represent a missing link in black hole growth, seeding the rapid formation of SMBHs in galaxies in the early Universe (e.g. Volonteri 2010). Theoretical studies have suggested that IMBHs may form in the dense environment found in the cores of globular clusters (GCs), for example from a supermassive star that forms via runaway stellar collisions during their early life (e.g. Portegies Zwart et al. 2004; Gieles et al. 2018b) or via mergers of BHs via gravitational wave inspiral over a period of Gyr (Giersz et al. 2015; Antonini, Gieles & Gualandris 2019). From simply extrapolating the observed relation between the black hole mass and the velocity dispersion of its host galaxy (Ferrarese & Merritt 2000; Gebhardt et al. 2000), one may expect black holes with masses characteristic of IMBHs to hide in GCs. If confirmed, observational evidence of IMBHs would also have a significant impact on a wide range of other astrophysical problems, from the origin of ultraluminous X-ray sources in nearby galaxies to the rates of gravitational wave events.

The quest to find IMBHs in the core of Milky Way GCs, where their presence has been debated for a long time, is however challenging. Deep radio observations of nearby GCs looking for signatures of accretion onto an IMBH have put upper limits on their masses of a several 100 to ~ 1000 M$_\odot$ (Strader et al. 2012b; Tremou et al. 2018), but these non-detections could be due to the paucity of gas in GCs at the present day. A lot of effort has thus focused on

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indirect dynamical inference to search for the presence of IMBHs, but to this day all reported detections remain contentious and inconclusive.

Earlier claims of IMBH detections in GCs are based on indications of a shallow central cusp in the surface brightness profile or a central rise in the velocity dispersion profile inside the sphere of influence of a putative IMBH (e.g. Newell et al. 1976; Noyola et al. 2008; Lützdorf et al. 2011), which is expected from relaxation arguments (Bahcall & Wolf 1976). All these findings have been rebutted, or at least questioned. In some cases, this was due to improvements in the measurements of the central velocity dispersion with discrete kinematics (proper motions or line-of-sight velocities for individual stars; van der Marel & Anderson 2010; Lanzoni et al. 2013) rather than integrated-light spectra which can be biased by stochasticity induced by bright stars (see e.g. Bianchini et al. 2015; de Vita et al. 2017). In other cases, there are other physical explanations that cannot be ruled out and are more plausible. Radially-biased anisotropy in the velocity distribution (Zocchi, Gieles & Hénault-Brunet 2017) or the presence of dark remnants such as white dwarfs, neutron stars (Illingworth & King 1977; den Brok et al. 2014) and BHs (Lützdorf, Baumgardt & Kruijssen 2013; Peuten et al. 2016; Zocchi, Gieles & Hénault-Brunet 2019; Baumgardt et al. 2019) can mimic the dynamical signatures previously ascribed to an IMBH, in particular the increase in the central velocity dispersion. The same goes for high-velocity stars found in the cores of some GCs (Meylan, Dubath & Mayor 1991; Gunn & Griffin 1979; Lützdorf et al. 2012), which may suggest interaction with an IMBH but can in fact simply result from interactions with a binary system (Lützdorf et al. 2012) or represent ‘potential escapers’, stars above the local escape velocity that are energetically unbound but trapped inside the Jacobi surface for several orbits before escaping the cluster (Fukushige & Heggie 2000; Clavelli, Gieles & Zocchi 2017; Daniel, Heggie & Vanri 2017).

Pulsar timing is a promising way to probe the gravitational potential of GCs and look for an IMBH in their core. Given the precise and stable clock provided by measurements of the period (spin or binary orbital period) of a pulsar, one can relate an observed change in that period (typically over a baseline of several years) to the gravitational acceleration from the cluster potential at the position of the pulsar. If there is no process intrinsic to the pulsar or binary system changing this period, then the observed period derivative is directly related to the gravitational acceleration along the line-of-sight (Phinney 1993; Prager et al. 2017). Perera et al. (2017) recently used long-term timing observations of the millisecond pulsar (MSP) PSR B1820\textendash{}30A, located less than 0.5\textquotedbl{} from the centre of NGC 6624, to argue for the presence of a central IMBH in that GC. Gieles et al. (2018a) however showed that the maximum line-of-sight acceleration at the position of the MSP is consistent with a mass segregated dynamical model of NGC 6624 without an IMBH. Baumgardt et al. (2019) also concluded that there is no need for an IMBH in NGC 6624 by comparing observations to N-body models with and without an IMBH.

Using spin period derivatives for 23 MSPs with timing solutions in 47 Tuc, Kızıltan, Baumgardt & Loeb (2017) argued for an IMBH with a mass $M_\text{BH} \sim 2200^{+150}_{-100} M_\odot$ in this cluster. To reach this conclusion, they compared the inferred pulsar accelerations (assuming an intrinsic spin-down distribution comparable to that of the Galactic field MSP population) to the accelerations of neutron stars in a grid of N-body simulations of GCs with and without an IMBH. Several assumptions could however have affected their analysis, for example the short distance to 47 Tuc of 4 kpc assumed by Kızıltan et al. (2017), whereas most recent estimates put it at ~ 4.5 kpc (Chen et al. 2018, and references therein). As pointed out by Mann et al. (2019), the N-body models of Kızıltan et al. (2017) do not have significant mass in binaries or other heavy objects (their main grid of models contained no primordial binaries and little or no stellar-mass black holes after a Hubble time). A lack of massive objects that would sink to the centre due to dynamical friction could lead to an underestimation of the gravitational acceleration in the central regions of their models without an IMBH. The assumption by Kızıltan et al. (2017) of a mass 1.4 $M_\odot$ for the MSPs (a lower limit on the true masses given that many of these are in binary systems; e.g. Freire et al. 2017) could also bias the comparison of the inferred accelerations of some pulsars with the distribution of accelerations in the N-body models since the adopted mass affects the predicted spatial distribution of these objects. Mann et al. (2019) used stellar proper motions from the Hubble Space Telescope (HST) in the core of 47 Tuc along with Jeans models to conclude that the measured central velocity dispersion profile provides no strong evidence for an IMBH, in particular if significant concentrated populations of heavy binary systems and dark stellar remnants are included.

This last point is particularly relevant given the recent interest in uncovering BH populations in GCs because of the detection of gravitational waves from merging BHs by LIGO (Abbott et al. 2016a). Dynamical formation of close BH-BH binaries in the dense cores of GCs could be one of the main formation channels for these mergers (e.g. Sigurdsson & Hernquist 1993; Portegies Zwart & McMillan 2000; Abbott et al. 2016b; Rodriguez et al. 2016). The amount of dynamically formed BH-BH binaries and eventual mergers in GCs as a function of time depends on several ingredients (e.g. the initial mass function – IMF, the initial-final mass relation, massive binary star evolution, the magnitude of natal kicks that BHs receive at birth, the dynamical age of the cluster, etc.), many of which are poorly constrained. A promising avenue to make progress is to quantify the size of BH populations in GCs today.

Radio and X-ray observations of GCs have led to the discovery of a few accreting stellar-mass BH candidates in mass-transferring binaries (e.g. Strader et al. 2012a), including one in 47 Tuc (Miller-Jones et al. 2015). Giesers et al. (2018) identified a detached stellar-mass BH candidate in the core of the Galactic GC NGC 3201 from the radial velocity variations of a main-sequence turn-off star companion. These findings suggest that the natal kick velocities of BHs can be low enough to retain at least a small fraction of the BHs formed in GCs. Since these types of binaries are rare (Kremer et al. 2018a), they could represent the tip of the iceberg of a much larger population of BHs that might be common in GCs but would have to be detected indirectly (for example through their dynamical signature).

Due to two-body relaxation and the trend towards kinetic energy equipartition, BHs (which are $\geq 10$ times more massive than the typical $\sim 0.5 M_\odot$ star in a GC) have a dynamical heating effect on cluster stars and tend to inflate the visible cluster core while suppressing mass segregation among observable stars in the cluster (e.g. Merritt et al. 2004; Mackey et al. 2008; Peuten et al. 2016). Based on relations between the number of BHs in GC models and

\footnote{Note that models from Kremer et al. (2018a) show little correlation between the presence of mass-transferring BH systems and the total number of BHs in the cluster at any given time; the net rate of formation of BH-non-BH binaries is largely independent of the total number of retained BHs. Should this lack of correlation generally hold true, one would not be able to estimate the total number of BHs in a GC by extrapolating from the number of known BH candidates in binaries.}
their global properties or kinematics, present-day populations of a few tens to a few hundreds of BHs have been proposed in several Milky Way GCs (e.g. Peuten et al. 2016; Kremer et al. 2018b, 2019; Askar et al. 2018). For 47 Tuc, Weatherford et al. (2018) inferred a population of ~ 20 BHs (but possibly as large as ~ 150 BHs within 2σ) based on the observed mass segregation between giants and low-mass main-sequence stars in the central regions of the cluster. There is however a need to confirm the predictions from these simple relations with more elaborate methods and/or by comparing models simultaneously to a wider range of observations of the internal kinematics and structural properties of GCs.

To shed light on the mass distribution and dark content of 47 Tuc, we present in this work a new self-consistent equilibrium multimass model of the cluster (without an IMBH) that captures the effect of mass segregation in the presence of dark stellar remnants. In Section 2, we present the various datasets to which we fit our models. We describe the multimass models and fitting procedure in Section 3 and the results of the fits in Section 4. We discuss the implications for the BH content, global present-day mass function and IMF of 47 Tuc in Section 5, and finally we summarize our conclusions in Section 6.

2 DATA

We summarize below the various datasets to which the models described in Section 3 are fitted, as well as additional data to which we compare predictions from our best-fitting models. In contrast to previous work that studied the mass distribution and black hole content of 47 Tuc focusing on one type of observable (e.g. either pulsar accelerations, the central velocity dispersion, or the observed mass segregation; Kiziltan et al. 2017; Mann et al. 2019; Weatherford et al. 2018, see Section 1), we simultaneously compare and fit our models to several observables that probe the mass distribution within the cluster and the phase-space distribution of objects of different masses.

2.1 Number density profile

To constrain the structural parameters of the cluster, we use the number density profile of 47 Tuc from the catalogue of de Boer et al. (2019), which is based on Gaia Data Release 2 (DR2) data, allowing accurate membership selection in the outer parts of the cluster. The profile is extended using supplemental literature data from surface brightness measurements (Trager et al. 1995) in the central regions of the cluster, where the completeness of Gaia data is affected by crowding. The Gaia number density profile is calculated from bright stars ($m > 0.6 M_\odot$) and the literature data are also dominated by bright stars. In both cases, the profile is dominated by stars from a narrow range of stellar masses (cf. de Boer et al. 2019). When fitting models, we thus assume that the number density profile traces the spatial distribution of upper main-sequence and evolved stars.

2.2 Kinematics

2.2.1 Proper motions

As the main constraint on the total mass of the cluster (and its distribution as a function of distance from the centre), we consider kinematic data from various sources. We use the HST proper motion dispersion profiles (tangential and radial components in the plane of the sky) in the central regions of the cluster from Watkins et al. (2015). These are based on cleaned samples of bright stars from the HST proper motion catalogs of Bellini et al. (2014) and only include stars brighter than the main-sequence turn-off.

We complement the dataset above with HST proper motion dispersion profiles of main-sequence stars from Heyl et al. (2017) in a field located further out and centered 6.7" in projection from the cluster centre (~ 8.8 pc, a little over two times the half-light radius; McLaughlin & van der Marel 2005). The mean mass of the stars in this dataset is 0.38 $M_\odot$ - significantly lower than the stars entering the other kinematic datasets - so inclusion of this dataset provides constraints on mass segregation and the mass dependence of kinematics. These data show evidence of radial anisotropy in the outer parts of 47 Tuc and provide a useful constraint on the anisotropy parameter (see Section 3). As shown by Zocchi et al. (2017), anisotropy in the outer regions of a cluster can influence the central velocity dispersion, with radially anisotropic models having a larger central dispersion (in the radial, tangential, and line-of-sight components) than the equivalent isotropic models. This ingredient was however not considered by Mann et al. (2019) who fitted isotropic Jeans models to the velocity dispersion profile in the core of the cluster. Given the different mass regime probed by these data compared to the other kinematic data used, they also provide additional leverage to capture and correctly model the effect of mass segregation.

For our main set of models, we adopt a distance of 4.45 kpc to convert model velocities to observed proper motions in units of mas yr$^{-1}$. This distance is the most recent and precise estimate ($4.45 \pm 0.01 \pm 0.12$ kpc; random and systematic errors, respectively) for 47 Tuc, obtained by Chen et al. (2018) using parallaxes from Gaia DR2 and taking advantage of the background stars in the Small Magellanic Cloud and quasars to account for parallax systematics. This distance also agrees with the recent dynamical distance of 4.4±0.1 kpc by Kamann et al. (2018). In Section 4, we will discuss how 2σ excursions from this adopted value of $D = 4.45$ kpc influence our results, and show that our main conclusions remain unaffected even with $D = 4.2$ kpc or $D = 4.7$ kpc.

2.2.2 Line-of-sight velocities

We also use the line-of-sight velocity dispersion profile of 47 Tuc from Baumgardt & Hilker (2018), which builds on a compilation of line-of-sight velocity measurements from Baumgardt (2017) and considers additional archival data. This includes several measurements from the literature (Mayor et al. 1983; Gebhardt et al. 1995; Carretta et al. 2009; Lane et al. 2011; Gratton et al. 2013; Da Costa 2016; Kunder et al. 2017; Kamann et al. 2018) which have been put on the same velocity scale by matching their mean radial velocity.

2.3 Stellar mass functions

In order to constrain the global stellar mass function of the cluster, we compare our models to measurements of the local stellar mass function in concentric annuli covering different ranges of projected distances from the cluster centre. Sollima & Baumgardt (2017) extracted stellar mass functions in four annuli within a projected radius of 1.6' from the centre of 35 GCs using the HST/ACS photometry published by the Globular Cluster ACS Treasury Project (Sarajedini et al. 2007). To convert magnitudes to stellar masses, they adopted the mass-luminosity relation of suitable isochrones from the Dotter et al. (2007) database. 47 Tuc was
not retained in the final sample analysed in Sollima & Baumgardt (2017), but stellar mass functions determined in the same way as for their 35 selected clusters were provided to us by A. Sollima (priv. comm.). These stellar mass functions for 47 Tuc are also presented in figure 2 of Baumgardt & Hilker (2018). The annuli cover the projected radius ranges $0.0' < R < 0.4'$, $0.4' < R < 0.8'$, $0.8' < R < 1.2'$, and $1.2' < R < 1.6'$. The mass range covered is $\sim 0.2 M_\odot < m < 0.85 M_\odot$ in the outermost of these four annuli but is narrower in the innermost annulus where crowding significantly affects the completeness of observations for the fainter low-mass stars.

Note that observations of the mass function in 47 Tuc were not considered in the analysis of Kiziltan et al. (2017), who argued in favour of an IMBH. These authors used $N$-body simulations of isolated star clusters with a Kroupa (2001) IMF (and hence no significant preferential loss of low-mass stars), despite the fact that previous work suggests a global stellar mass function depleted in low-mass stars for this cluster (e.g. Giersz & Heggie 2011). This could have affected their inferred mass distribution, and hence the predicted pulsar accelerations on which their conclusions are based.

### 2.4 Pulsar data

Although we do not directly include them in the fitting procedure, we consider the spatial distribution and inferred accelerations of pulsars in 47 Tuc as additional observables that are compared to our best-fitting models to serve as a consistency check. Because pulsars have a higher mass than our tracer stars and their accelerations probe the gravitational potential of the cluster, these data help to assess the validity and predictive power of our models fitted to the number density profile, kinematics, and stellar mass function data.

Freire et al. (2017) presented updated or new long-term timing solutions for the majority of the 25 known millisecond pulsars in 47 Tuc based on data from the Parkes 64-m radio telescope. To compare with the maximum line-of-sight accelerations predicted by our models, we take the orbital period derivatives and associated inferred line-of-sight accelerations ($\dot{P}_\text{los}$) to the observed period derivative) for 10 binary systems with a timing solution and measured orbital period derivative (Ridolfi et al. 2016 for 47 Tuc X, Freire et al. 2017 for the nine other binary systems: 47 Tuc E, H, I, Q, R, S, T, U, and Y). Two of these (47 Tuc I and R) are black-widow systems with a low-mass companion ($< 0.05 M_\odot$) and the others have a white dwarf companion. For the remainder of the MSPs with a timing solution (either isolated pulsars or binaries for which the orbital period derivative could not be measured), we compute an upper limit on the line-of-sight acceleration from the measured first spin period derivative ($\dot{P}_\text{los} < c P_{\text{spin}}/P_{\text{spin}}$; with measurements from Freire et al. 2017, Ridolfi et al. 2016, and Freire & Ridolfi 2018).

From the coordinates of all of the above MSPs, plus two additional ones without a timing solution (47 Tuc P and V; e.g. Ridolfi et al. 2016), we build a cumulative radial distribution of MSPs in 47 Tuc which we use as a proxy for the spatial distribution of neutron stars in the cluster and an additional sanity check for our mass segregated models. We adopt the position of the cluster centre determined by Goldsbury et al. (2010).

### 3 MODELS AND FITTING PROCEDURE

#### 3.1 Multimass dynamical models

To model the mass distribution within 47 Tuc, we use the multimass version of the limepy2 family of dynamical models (Gieles & Zocchi 2015). These models are based on a distribution function that approximates an isothermal sphere for the most bound stars in the central regions and is described by polytropes in the external regions near the escape energy. The latter aspect allows to describe dynamically evolved and tidally limited systems and approximately capture the effect of the galactic tidal field on the structure and dynamics of GCs in the simplifying assumption of spherical symmetry. The truncation parameter $g$ (related to the polytropic index $n = g + 1.5$) sets the sharpness of the truncation in energy: models with larger values of $g$ are more extended and have a less abrupt truncation. The concentration of the models is controlled by the dimensionless central potential $W_0$, similar to the concentration parameter of King (1966) models. limepy models with $g = 1$ are single-mass King models, while models with $g = 0$ are Woolley (1954) models and those with $g = 2$ the also well-known isotropic and non-rotating Wilson (1975) models. Note that any intermediate value of $W_0$ depends on the definition of the mean mass, and we adopt here the global mean mass of the entire model (for details on this and alternative definitions, see Peuten et al. 2017). The distribution function of the limepy models includes an angular momentum term that allows to include Michie-type anisotropy (isotropy in the centre of the cluster, radially anisotropic velocity distribution in the intermediate parts, and isotropy again near the truncation radius; Michie 1963). This is specified by the anisotropy radius ($r_a$) parameter, which sets the amount of velocity anisotropy in the system: models with a small $r_a$ are radially anisotropic, while models with a large $r_a$ (with respect to the truncation radius) have an isotropic velocity distribution everywhere. This form of anisotropy profile has been shown to satisfactorily describe globular clusters evolving in an external tidal field in $N$-body simulations (Sollima et al. 2015; Zocchi et al. 2016; Tiongco et al. 2016). Peuten et al. (2017) showed with $N$-body models that in the early evolution $r_a$ is smaller for the lower-mass objects and in the late stages of evolution it is the more massive stars and remnants that have a smallest $r_a$. For the present-day dynamical age of 47 Tuc (Giersz & Heggie 2011), the results of Peuten et al. (2017) suggest that $r_a$ is approximately independent of mass, hence we proceed with the assumption that anisotropy for all mass bins can be described by a single value of $r_a$.

Multiple mass components and the effect of mass segregation between these components are included in the limepy models by relating the velocity scale of each mass component ($v_s$) to the mass of the component ($m_s$) as $v_s \propto m_s^{\delta}$ (where $\delta$ is usually set to 1/2; see Gunn & Griffin 1979). This formulation leads to equipartition at high masses, but to a shallower mass dependence of the central velocity dispersion at lower masses which matches what is seen in $N$-body and Monte Carlo simulations of GCs (e.g. Gieles & Zocchi 2015; Bianchini et al. 2016; Peuten et al. 2017). We emphasize that the limepy models have been extensively tested against snapshots from direct $N$-body simulations for which the full phase-space information is available, including that of different mass components in simulations with a mass spectrum (Zocchi et al. 2016; Peuten

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2 A PYTHON solver allowing to compute models is available at [https://github.com/mgieles/limepy](https://github.com/mgieles/limepy)
et al. 2017). In particular, Peuten et al. (2017) showed that multiform IMEY models accurately reproduce the degree of mass segregation in evolved multimass systems in different tidal fields and with vastly different populations of dark remnants (e.g. from no neutron stars and BHs to a large retention fraction of stellar-mass black holes).

In addition to the three parameters introduced above \( (W_0, g \text{ and } r_0) \) and the mean stellar mass \( (m_i) \) and total mass \( (M_f) \) of each of the different mass components, two physical scales must be specified to compute a model that can be compared to observations. We adopt here the total cluster mass \( (M) \) and half-mass radius \( (r_h) \) as the additional parameters specifying those scales.

### 3.2 Stellar mass function and remnants

To determine the individual values of \( m_j \) and \( M_f \), we define four additional free parameters associated with the global mass function within the cluster. An initial mass function is adopted and defined by a three-component broken power law \( (dN/dm \propto m^{-a}) \) with break masses at \( m = 0.5 \, M_{\odot} \) and \( m = 1 \, M_{\odot} \), and power-law indices \( a_1 \), \( a_2 \) and \( a_3 \) corresponding to the low, intermediate, and high-mass ranges, respectively. We evolve this mass function to the present day assuming a metallicity of \( [\text{Fe}/\text{H}] = -0.7 \) and an age of 11 Gyr (Dotter et al. 2010; Hansen et al. 2013) to turn higher mass stars into white dwarfs, neutron stars, and black holes following the mass function evolution algorithm from Balbinot & Gieles (2018), updated by Peuten et al. (in prep.) to include a more realistic treatment of the initial-final mass relation for the different types of remnants (e.g. Dotter 2016; Belczynski et al. 2008). Modification of the mass function by dynamical evolution and preferential escape of low-mass stars and remnants is assumed to be negligible for 47 Tuc (see Section 5.2), so this effect is not included in our models and fitting procedure. We note that Monte Carlo models by Giersz & Heggie (2011) suggest that almost 50% of the mass of the cluster has been lost, but this is due to stellar evolution mass loss, i.e. high mass stars turning into remnants, and not escaping low-mass stars.

We allow for a varying retention fraction of the number of BHs (\( BH_{\text{ret}} \)), removing the more massive BHs first as expected for a slow depleton of the BH reservoir from dynamical ejections, where the more massive BHs have a larger dynamical interaction cross-section (Morscher et al. 2015; Antoniè & Gieles 2019). This approach implicitly assumes a 100% BH retention after supernovae, which is justified given the estimates of the total initial mass and escape velocity at formation of 47 Tuc (see Giersz & Heggie 2011, and Section 5.3). For the neutron stars, we make the common assumption of a retention fraction of 10% (e.g. Pfahl et al. 2002), but our results are actually insensitive to the precise retention fraction of neutron stars adopted (see Section 4). Our mass function evolution algorithm assigns objects into discrete mass bins, with stars distributed over 30 logarithmically spaced mass bins at time \( t = 0 \). Depending on the BH retention, the mass function consists of 15-19 mass bins at the present day.

Combined with the total cluster mass \( (M) \), the four additional free parameters (power-law exponents \( a_1, a_2, a_3 \), and \( BH_{\text{ret}} \)) fully define the mass function, allowing to specify all values of \( m_j \) and \( M_f \) needed to build the multimass model.

When fitting multimass models similar to the ones described here to mock data from an N-body simulation, Hénault-Brunet et al. (2019) found that the fraction of the cluster mass in dark remnants and even the mass function of the remnants can be reliably recovered and constrained. Thanks to the trend towards equipartition between objects of different masses, the phase-space distribution of tracer stars is sensitive to the dark remnants, allowing to probe the BH content and the IMF above the present-day main-sequence turnover mass.

### 3.3 Fitting procedure

For the models described in the previous subsections, we have a total of 12 free parameters, including the following: \( W_0, g, \log r_0, M, r_h, a_1, a_2, a_3, BH_{\text{ret}}, \) and \( \delta \) defined as above. The two additional parameters are nuisance parameters that capture otherwise unaccounted-for observational uncertainties or limitations of the model for the density profile \( (s^2) \) and the mass function \( (F) \), as described below.

To compare a given model to the datasets described in Sections 2.1 to 2.3, we compute the likelihood of each observational data point given the model parameters. We assume a Gaussian likelihood for all the observables, with the standard deviation \( \delta \) given by the uncertainties (observational, plus in some cases an additional component captured by a nuisance parameter). The likelihood of an observed line-of-sight velocity dispersion \( \sigma_{\text{LOS},i} \) with its uncertainty \( \delta \sigma_{\text{LOS},i} \) at projected distance \( R \) from the centre, given model parameters \( \Theta \), is

\[
L_{\text{LOS}_{i}}(\sigma_{\text{LOS}_{i}}(R), \delta \sigma_{\text{LOS}_{i}}(R) | \Theta) = \frac{1}{\sqrt{2\pi \delta \sigma_{\text{LOS}_{i}}(R)^2}} \exp\left(-\frac{1}{2} \left(\frac{\sigma_{\text{LOS}_{i}}(R) - \sigma_{\text{LOS}_{i}}(R)}{\delta \sigma_{\text{LOS}_{i}}(R)}\right)^2\right),
\]

where \( \sigma_{\text{LOS}_{i}}(R) \) is the model line-of-sight velocity dispersion at the distance \( R \). Since the line-of-sight velocity dispersion data is dominated by giants, we use the mass bin corresponding to the most massive upper main-sequence stars for the model line-of-sight velocity dispersion to compare with the data.

Similarly, for the HST proper motion dispersion data in the central regions of the cluster from Watkins et al. (2015), the likelihood of an observed proper motion dispersion in the radial direction \( \sigma_{\text{pmR},i} \) with its uncertainty \( \delta \sigma_{\text{pmR},i} \) at projected distance \( R \) from the centre, given model parameters \( \Theta \), is

\[
L_{\text{pmR}_{i}}(\sigma_{\text{pmR}_{i}}(R), \delta \sigma_{\text{pmR}_{i}}(R) | \Theta) = \frac{1}{\sqrt{2\pi \delta \sigma_{\text{pmR}_{i}}(R)^2}} \exp\left(-\frac{1}{2} \left(\frac{\sigma_{\text{pmR}_{i}}(R) - \sigma_{\text{pmR}_{i}}(R)}{\delta \sigma_{\text{pmR}_{i}}(R)}\right)^2\right).
\]

For the MUSE data from Kamann et al. (2018) which are included in the line-of-sight velocity dispersion profile compiled by Baumgardt & Hilker (2018), this assumption is not entirely accurate. Because of the different stellar densities, longer exposure times were used when observing the outer MUSE fields. Hence, in the outermost bins of the MUSE observations the kinematics trace different stars than in the innermost bins. For 47 Tuc, the difference in the effective stellar mass traced over the spatial extent of the MUSE data is however only \( \sim 0.1 \, M_{\odot} \), so this does not have a significant impact on the results.
where \( \sigma_{\text{pat},i}(R) \) is the model proper motion dispersion at the distance \( R \) in the radial direction. The likelihood of an observed proper motion dispersion in the tangential direction \( \sigma_{\text{tang},i}(R) \), with its uncertainty \( \delta \sigma_{\text{tang},i}(R) \), at projected distance \( R \) from the centre, given model parameters \( \Theta \), is

\[
L_{\sigma_{\text{tang},i}}(\sigma_{\text{tang},i}(R), \delta \sigma_{\text{tang},i}(R) \mid \Theta) = \frac{1}{\sqrt{2\pi}\delta \sigma_{\text{tang},i}(R)} \exp\left(-\frac{1}{2} \frac{\left(\sigma_{\text{tang},i}(R) - \delta \sigma_{\text{tang},i}(R)\right)^2}{\delta \sigma_{\text{tang},i}(R)^2}\right),
\]

where \( \sigma_{\text{pat},i}(R) \) is the model proper motion dispersion at the distance \( R \) in the tangential direction. Since these proper motion data only include stars brighter than the main-sequence turn-off, we again use the mass bin corresponding to the most massive upper-main-sequence stars for the model proper motion dispersion to compare with the data. Evolved phases like red giant branch (RGB) and asymptotic giant branch (AGB) stars are expected to have a very similar mass and to behave dynamically like stars with a mass comparable to the mass of turn-off stars. In particular, for 47 Tuc, Parada et al. (2016) conclude that the post-main-sequence mass loss occurs at the end of the AGB phase, so the mass remains constant for stars going through the evolutionary stages from the upper main-sequence up to the horizontal branch. Their slightly higher mass estimates for AGB stars are consistent with the AGB having evolved from somewhat more massive stars.

For the proper motion dispersion observations from Heyl et al. (2017), the likelihood is defined in the same way as in equations (2) and (3). The median mass of the stars in this dataset is 0.38 M\(_\odot\), so we use the mass bin with the corresponding lower mean mass \( m_i \) for the model proper motion dispersion to compare with these data, and we refer to the likelihood of an observed proper motion dispersion as \( L_{\sigma_{\text{pat},i}} \) and \( L_{\sigma_{\text{tang},i}} \), respectively for the radial and tangential components. We note that the median mass of 0.38 M\(_\odot\) is based on a sample of stars from a relatively wide magnitude or mass range (24 > \( \text{F814W} \) > 18; 0.2 \( \geq m_i/M_\odot \) \( \geq 0.8 \)), and the velocity dispersion from this whole sample is not necessarily exactly the same as the dispersion of stars with this median mass because the velocities are mass-dependent. We thus also considered a separate test case where we fitted these proper motion dispersion data by using as a reference a lower-mass bin in our models (\( m_j = 0.3 M_\odot \)), which may be representative of the mean kinematics of the sample considered (cf. Fig. 6 and Fig. 7 from Heyl et al. 2017). We conclude in Section 4 that this does not significantly affect our results, since the difference in the velocity dispersion is very small (\( \leq 0.3 \text{ km s}^{-1} \)) for this small difference in tracer mass in this outer field.

The number density profile from de Boer et al. (2019) is compared to the model prediction for the heaviest main-sequence stars. We include in our model density profile a constant background level of 0.08 arcmin\(^{-2}\) to match the data in the very outskirts of the cluster. To let the total mass be constrained by the kinematics and stellar mass functions, we only fit on the shape of the profile and not on the absolute values. The likelihood of a measured number density \( \Sigma_j(R) \) and its uncertainty \( \delta \Sigma_j(R) \) at the projected distance \( R \), given model parameters \( \Theta \), is

\[
L_{\Sigma_j}(\Sigma_j(R), \delta \Sigma_j(R) \mid \Theta) = \frac{1}{\sqrt{2\pi}\delta \Sigma_j(R)} \exp\left(-\frac{1}{2} \frac{(\Sigma_j(R) - \delta \Sigma_j(R))^2}{\delta \Sigma_j(R)^2}\right),
\]

where \( \Sigma_j(R) \) is the predicted number density from the model at the distance \( R \) in the heaviest main-sequence mass bin. \( K \) is the scaling parameter that minimizes the vertical offset between the model and observed profile. It re-scales the model profile and allows to fit only on the shape of the number density profile, not its absolute values. It is derived from setting the derivative of the \( \chi^2 \) expression \( \sum_{i=1}^{N_i} (K \Sigma_j(R) - \delta \Sigma_j(R))^2 / \delta \Sigma_j(R)^2 \) with respect to \( K \) equal to zero and is defined as

\[
K = \frac{\sum_{i=1}^{N_i} \Sigma_j(R) \Sigma_j(R) / \delta \Sigma_j(R)^2}{\sum_{i=1}^{N_i} \delta \Sigma_j(R)^2 / \delta \Sigma_j(R)^2},
\]

where the sums are over all \( N_i \) data points in the binned observed density profile. In the uncertainty on the observed number density profile (\( \delta \Sigma_j(R) \)), we include both the formal uncertainty from de Boer et al. (2019), \( \delta \Sigma_j(R) \), and an additional unknown uncertainty encapsulated by nuisance parameter \( s^2 \) such that \( \delta \Sigma_j(R)^2 = \delta \Sigma_j(R)^2 + s^2 \). This nuisance parameter adds a constant component to the uncertainty over the entire extent of the observed number density profile. This effectively allows small deviations between the model and observations in the outer parts of the cluster, for example to account for the effect of potential escapers (Claydon et al. 2017, 2019) which are not captured by multimass \textsc{limopy} models in their current implementation (cf. Hénault-Brunet et al. 2019).

For the comparison of the models and mass function data, we write down the likelihood of an observed number of stars per unit mass \( N_j \) with its uncertainty \( \delta N_j \) at mass \( m \) in a given field, given model parameters \( \Theta \), as

\[
L_{\text{MF}}(N_j(m), \delta N_j(m) \mid \Theta) = \frac{1}{\sqrt{2\pi}\delta N_j(m)} \exp\left(-\frac{1}{2} \frac{(N_j(m) - \delta N_j(m))^2}{\delta N_j(m)^2}\right),
\]

where \( N_j(m) \) is the number of stars per unit mass at mass \( m \) predicted by the model in the same region. The likelihood for the observed mass function in a given field is the product of the individual likelihoods of all measurements at different masses in that field (\( L_{\text{MF}} = \Pi_i L_{\text{MF}}(\cdot) \)). We compute the likelihood for the observed mass function given the model parameters in the four different annular regions mentioned above (\( L_{\text{MF},0.4-0.8}, L_{\text{MF},0.8-1.2}, L_{\text{MF},1.2-1.6'} \)).

In the uncertainty on the observed number of stars per unit mass (\( \delta N_j(m) \)), we include both the Poisson error on the number of stars (\( \delta N_j(m) \)) and an additional unknown uncertainty captured by the nuisance parameter \( F \) and expressed as a fraction between 0 and 1, such that \( \delta N_j^2 = \delta N_j^2 + (F N_j)^2 \). This nuisance parameter encapsulates possible additional sources of uncertainty like errors in the completeness correction of the photometric dataset from which the mass functions were extracted, or limitations of the assumed broken power-law functional form for the underlying global mass function, which may not be a perfect representation of the mass function of the cluster.

For each dataset, we multiply the individual likelihoods for different data points to obtain the likelihood of this dataset given the model. We then multiply the likelihoods for different datasets to obtain the total likelihood:

\[
L_{\text{tot}} = L_{\text{tot},0.4-0.8} L_{\text{tot},0.8-1.2} L_{\text{tot},1.2-1.6'}
\]

Using the total likelihood function above (in practice we maximize the log-likelihood and can conveniently sum individual log-likelihoods for the different datasets to get the total log-likelihood),
we determine the posterior distributions of the model parameters using the Markov Chain Monte Carlo sampler emcee (Foreman-Mackey et al. 2013), adopting uniform priors on all parameters (for the anisotropy radius we actually fit on log (r_\text{e})). The ranges considered for these uniform priors are listed in Table 1.

4 RESULTS

4.1 Best-fitting model and parameters

We show in Fig. 1 the resulting model fit to the number density profile, kinematics, and local stellar mass functions. The error bars displayed for the number density profile and mass function data include the error contributions captured by the associated nuisance parameters. Fig. 2 shows the corresponding marginalised posterior probability distribution and 2D projection of the posterior probability distribution for each fitting parameter and pair of parameters. The posterior probability distributions are all well confined within the adopted prior ranges and appear mostly unimodal. The best-fit model parameters and associated uncertainties (i.e. the median and ±1σ uncertainties - corresponding to the 16th and 84th percentiles of the marginalised posterior probability distribution) are listed in Table 1. Note that the best-fitting model (continuous lines) and credible intervals (shaded regions) shown in Fig. 1 do not correspond directly to models computed from the best-fitting values of Table 1, but rather they are computed from the 16th, 50th, and 84th percentiles (at a given radius or mass) of the profiles computed by sampling parameters from the posterior distribution.

All the different observables considered in the fit are satisfactorily reproduced by the best-fitting model. Some small deviations are found between the best-fitting model and data, but the vast majority are within 2σ, apart from the outermost line-of-sight velocity dispersion data points where the model underestimates the observed velocity dispersion (this is in the regime where we may expect potential escapees, not included in our model, to slightly inflate the velocity dispersion). We note that additional physical ingredients like rotation could eventually be included in the modelling to obtain an even better and complete description of the cluster; 47 Tuc indeed displays significant rotation (e.g. Bellini et al. 2017). Obtaining an even better and complete description of the cluster; 47 Tuc indeed displays significant rotation (e.g. Bellini et al. 2017). On the black hole content and IMF of 47 Tuc also degenerate with the amount of anisotropy, a consequence of the well-known mass-anisotropy degeneracy. Both a larger retention of black holes and a larger amount of radial anisotropy increases the central velocity dispersion (e.g. Zocchi et al. 2017, 2019).

Our best-fitting mass segregation parameter (δ = 0.44 ± 0.02) is close to the commonly adopted value of δ = 0.5. The resulting relation between the central velocity dispersion and mass (in the range ∼ 0.4–0.8 M_⊙) is shallower (σ (r = 0) ∝ m^{−0.38}). In projection our model gives: σ^2(R = 0) ∝ m^{-0.32}.

Comparing to the results of Baumgardt & Hilker (2018) who fitted their grid of N-body models to similar data for 47 Tuc, we find a half-mass radius that is ~ 30% larger and a total cluster mass that is ~ 25% larger (both significantly different than allowed by the statistical errors on the fits of the two studies). We note that the ratio M/σ_v, which is proportional to the velocity dispersion squared, is very similar in both models. Part of the difference in mass may be traced to the shallower present-day mass function inferred by these authors, who find a power-law slope of α = −0.53 over the mass range 0.2 M_⊙ < m < 0.8 M_⊙. Our mass function, with a break at 0.5 M_⊙, is comparable below 0.5 M_⊙ but steeper above this break mass and thus contains a larger proportion of low-mass stars which would be preferentially distributed in the outer parts of the cluster and could increase the inferred total mass and half-mass radius without significantly affecting the mass profile in the inner regions. Moreover, our total likelihood function includes a comparison with radial and tangential proper-motion data that provide constraints on the radial anisotropy in 47 Tuc, whereas such data is not included in the fits of Baumgardt & Hilker (2018) - anisotropy cannot be freely varied in their grid of N-body models. It is possible that their best-fitting model has too much radial anisotropy, which would then require less mass to fit the central velocity dispersion and could lead to underestimating the cluster mass or their models have less mass in the outer parts. An other explanation could be that the visible stars are more segregated towards the centre in our models because we allowed δ to be free. A direct comparison between the models would be required to understand the differences.

4.2 Radial distribution and line-of-sight accelerations of millisecond pulsars

Fig. 3 shows the cumulative radial distribution of the 25 known MSPs (Freire et al. 2017; Ridolfi et al. 2016; Freire & Ridolfi 2018) in 47 Tuc (black line) compared to the prediction of our best-fitting multimass models for a 1.6 M_⊙ tracer (the typical mass of MSP systems in 47 Tuc given the presence of binary companions in a fraction of the systems. We assume a mass of 1.4 M_⊙ for the isolated pulsars). We emphasize that these data were not included in our model fit and that only observables probing the phase-space distribution of visible stars below ~ 0.85 M_⊙ were used to constrain the free parameters of the model. Thus, the remarkable agreement between the data and model predictions lends further support to the ability of our models to reliably reproduce the underlying distribution of objects of different masses, including heavy dark remnants.

As discussed in Section 1, long-term timing of millisecond pulsars can also be used to probe the gravitational potential of a globular cluster. Ignoring intrinsic effects modifying the period (spin or orbital) of the MSP, this period and its derivative can be linked to the line-of-sight gravitational acceleration within the cluster potential as P/P = a_{los}/c (Phinney 1993; Prager et al. 2017), where c is the speed of light (a positive a_{los}, i.e. away from the observer, leads to an apparent spin-down or growth of the period). In the presence of an unknown intrinsic spin-down (e.g. due to mag-
The inferred acceleration is an upper limit to the true acceleration from the cluster potential. If the intrinsic component is known, the acceleration can be computed as $a_{\text{los}}/c = (\dot{P}/P)_{\text{meas}} - (\dot{P}/P)_{\text{int}}$, where the ‘meas’ and ‘int’ subscripts refer to the measured and intrinsic period derivatives. Additional terms, for example the acceleration due to the Galactic potential and the proper motion, are usually negligible (Phinney 1993).

Fig. 4 compares inferred line-of-sight accelerations for MSPs in 47 Tuc to the maximum (positive) and minimum (negative) line-of-sight accelerations predicted by our best-fitting multimass model as a function of projected distance from the centre of the cluster. We split the sample of inferred accelerations into two subgroups following the data presented in Section 2.4: (1) line-of-sight accelerations determined from the orbital period derivatives of 10 MSPs in binary systems, which we assume are directly probing the acceleration in the cluster because the intrinsic orbital period derivative should be negligible, and (2) upper limits on the line-of-sight accelerations based on the spin period derivatives of the other 13 MSPs, which could have a non-negligible (but currently unknown) intrinsic spin-down component, hence the upper limit. We see from Fig. 4 that all upper limits from the latter subgroup are safely above the minimum (negative) line-of-sight acceleration allowed by our best-fitting model and scattered between the maximum (positive) and minimum (negative) acceleration boundaries. The true accelerations determined for the 10 binary systems are also in good agreement with our model. They all fall within the boundaries allowed by the model within $1\sigma$, except for one system (47 Tuc S) which is
Figure 2. Marginalised posterior probability distribution and 2D projections of the posterior probability distribution of the fitting parameters for the limepy multimass model fit to 47 Tuc observations. Contours indicate 1, 2 and 3σ levels on the 2D posterior probability distributions.

however still consistent within less than 1.5σ. The majority of the accelerations for these binary systems cluster around the maximum and minimum boundaries. We note that this is not unexpected; the probability distribution of the acceleration at a given projected distance from the centre peaks near these boundaries as a result of the density distribution of the cluster and the variation with line-of-sight distance of the component of the acceleration vector that is projected along the line of sight. The good agreement between the MSP data and our mass model lends confidence to our choice of model and associated assumptions. A more in-depth statistical analysis of the pulsar accelerations and associated constraints on the mass profile and BH content of 47 Tuc will be presented in a future work.

4.3 Global present-day mass function and IMF

We highlight in Fig. 5 the marginalized posterior probability distribution for each of the three power-law exponents defining the (initial) stellar mass function in 47 Tuc. The inferred global mass function for low-mass stars is significantly flatter than a canonical IMF (Kroupa 2001), with $\alpha_1 = 0.52^{+0.17}_{-0.16}$ and $\alpha_2 = 1.35^{+0.25}_{-0.23}$ compared to $\alpha_1 = 1.3$ and $\alpha_2 = 2.3$ for the Kroupa IMF in the same
Table 1. Best-fitting model parameters and associated uncertainties (i.e. the median and ±1σ uncertainties - corresponding to the 16th and 84th percentiles of the marginalised posterior probability distribution) for our multimass model fit to 47 Tuc data.

| Parameter | Value       | Prior range |
|-----------|-------------|-------------|
| \( W_0 \) | 6.1±0.2     | (3, 20)     |
| \( g \)   | 0.57±0.07   | [0, 2.3]    |
| \( \log r_s/\text{pc} \) | 1.23±0.02 | [0.5, 15] |
| \( M/10^6 \, M_\odot \) | 1.06±0.01 | [0.01, 10] |
| \( n_0/\text{pc} \) | 8.16±0.12 | [0.5, 15] |
| \( \sigma_1 \) | 0.52±0.17 | [-2, 6]  |
| \( \sigma_2 \) | 1.35±0.25 | [-2, 6]  |
| \( \sigma_3 \) | 2.49±0.08 | [-2, 6]  |
| \( BH_{\text{ret}} \) | 0.59±0.06% | [0, 100%] |
| \( \delta \) | 0.44±0.02 | [0.3, 0.5] |
| \( F \) | 0.21±0.04 | [0.5]  |
| \( \sigma^2 \) | 0.01±0.01 | [0, 10]  |

Figure 3. Cumulative radial distribution of the 25 known MSPs in 47 Tuc (black line) compared to the prediction of our best-fitting multimass models for a 1.6 \( M_\odot \) tracer (the typical mass of MSP systems in 47 Tuc given the presence of binary companions in a fraction of the systems). The 1σ and 2σ credible intervals of the model distribution for these objects are shown with dark and light shaded green regions, respectively.

Figure 4. Line-of-sight gravitational acceleration of pulsars as a function of projected distance from the centre of 47 Tuc. The green envelope bounds the maximum (positive) and minimum (negative) line-of-sight acceleration at a given projected distance from the centre, based on the mass distribution of our best-fitting multimass model. Red circles show line-of-sight accelerations inferred from the measured orbital period derivative of 10 MSPs, while blue inverted triangles show upper limits on the line-of-sight acceleration in the field of the cluster for another 13 MSPs based on their spin-period derivative (which could have an intrinsic spin-down component, hence the upper limit on the real acceleration in the field of the cluster).

4.4 Model assumptions and uncertainties

In addition to the results presented above, for which a distance of 4.45 kpc was adopted (Chen et al. 2018), we also repeated the fitting procedure by assuming distance values of \( D = 4.2 \) kpc and \( D = 4.7 \) kpc (2σ excursions from the value of Chen et al. 2018). This mainly affected the inferred mass, radius, and some of the mass function slopes, although not in a major way. All other model parameters and inferred secondary quantities (including the mass in BHs; see discussion below) remained the same within 1σ uncertainties. For \( D = 4.2 \) kpc, the inferred \( n_0 \) decreased to 7.4±0.1 pc and the inferred cluster mass decreased to 0.88±0.01 \( 10^6 \, M_\odot \). On the other hand, for \( D = 4.7 \) kpc, the inferred \( n_0 \) increased to 8.7±0.1 pc and the inferred cluster mass increased to 1.20±0.01 \( 10^6 \, M_\odot \). Either way, the effect on the radius is less than 10% and the effect on the cluster mass less than 20%. While \( \alpha_1 \) changed by less than 0.1 when adopting the two extreme distance values, the other power-law exponents were more significantly affected: \( \alpha_2 = 1.74^{+0.27}_{-0.27} \) and \( \alpha_3 = 2.21^{+0.10}_{-0.10} \) for \( D = 4.2 \) kpc, whereas \( \alpha_2 = 1.06^{+0.29}_{-0.29} \) and \( \alpha_3 = 2.64^{+0.07}_{-0.06} \) for \( D = 4.7 \) kpc. Our conclusion that the low-mass mass function is significantly flatter than a Kroupa IMF is therefore robust and not strongly affected by uncertainties on the distance.

We also performed fits assuming different retention fractions for the neutron stars, with anywhere from zero to several thousands of neutron stars retained, and found that all the best-fitting parameters remained unchanged within 1σ uncertainties. Similarly, adopting a lower mass of 0.3 \( M_\odot \) (compared to 0.38 \( M_\odot \)) for the model tracer stars to be compared with the proper motion data from Heyl...
On the black hole content and IMF of 47 Tuc

Figure 5. Marginalised posterior probability distribution (blue shaded histograms) for each of the three power-law exponents defining the (initial) stellar mass function in 47 Tuc, for the ranges $m < 0.5 \, M_\odot$ ($\alpha_1$), $0.5 < m < 1 \, M_\odot$ ($\alpha_2$), and $m > 1 \, M_\odot$ ($\alpha_3$). For each distribution, the median is shown by a solid blue vertical line and the 1σ uncertainties (16th and 84th percentiles) by the dashed dotted blue lines. For reference, we also show vertical lines with the slopes for the Kroupa (dash-dotted green lines) and Salpeter (grey dashed lines) in the corresponding mass range. The tension with a standard IMF is clear in the low-mass regime.

et al. (2017) did not significantly change any of the best-fitting parameter values.

We finally recall that we have assumed that modification of the mass function by dynamical evolution and preferential escape of low-mass stars and remnants is negligible for 47 Tuc. When varying the mass function at low masses, we therefore assume that this corresponds to variations in the IMF. Note that if the IMF was actually normal and was dynamically depleted of low-mass stars by some dynamical effect not considered, then the low-mass end of the white dwarf mass function would also be affected (e.g. see Fig. 2 from Gieles et al. 2018a). This may require a somewhat flatter high-mass IMF to end up with the same mass in remnants, but it is not immediately clear precisely how this would affect the mass model.

5 DISCUSSION

5.1 Black holes in 47 Tuc

5.1.1 No need for an IMBH

Our best-fitting multimass model of 47 Tuc can naturally accommodate the accelerations of MSPs in this cluster, without invoking the presence of a central IMBH. The good agreement between the model and a range of observational constraints suggests that an IMBH is not needed given the data currently available (see also Mann et al. 2019). Kızıltan et al. (2017) reached a different conclusion when using the spin-period derivatives of pulsars (along with an assumed intrinsic spin-down distribution to infer accelerations) as the sole observable to distinguish between models with and without an IMBH; their models favoured an IMBH with a mass $M_\bullet \sim 2200^{+1500}_{-800} \, M_\odot$. It is unclear which assumption(s) in their analysis (see Section 1) could have led to this different result, but we note that it is based on a grid of isolated N-body models that would have a much steeper present-day mass function, closer to a Kroupa (2001) IMF and the assumption of a shorter distance. In Section 4.4 we showed that adopting a shorter distance leads to a shallower IMF slopes at high masses. This suggests that the data then prefers additional dark mass in the centre in the form of remnants, which might explain the need for an IMBH in the analysis of Kızıltan et al. (2017).

5.1.2 Constraints on the stellar-mass BH population

From the constraints on the mass function, total cluster mass and black hole retention fraction provided by our multimass model fit, we can recover the probability distribution for the total mass in BHs at the present day in 47 Tuc (Fig. 6). We find a preference for a population of BHs with a total mass of $430^{+386}_{-301} \, M_\odot$, or equivalently $141^{+97}_{-95} \, BH$s with a mean mass of $3^{+0.4}_{-0.4} \, M_\odot$ given our assumptions impacting the BH mass function (where our average BH mass is low because we assume massive BHs are dynamically ejected). The BHs contribute $\sim 10^4 \, M_\odot$ pc$^{-3}$ to the central mass density of the cluster, which we infer to be $\sim 10^5 \, M_\odot$ pc$^{-3}$ from our best-fitting models. While the BH contribution to the central density is not dominant, it is much more important (thanks to mass segregation) than one might guess from the very small fraction of
the cluster mass in BHs (\( \lesssim 0.1\% \)). This makes our models sensitive to a relatively small BH population and allows us to place the useful constraints above.

Our results are also consistent with a negligible number of BHs within \( \sim 1.5 r_c \). This is in agreement with the 19 BHs retained in the Monte Carlo model of 47 Tuc by Giersz & Heggie (2011), although we note that their results are based on a limited number of Monte Carlo models (the study indeed does not claim a full exploration of the parameter space for the cluster initial conditions and the retention of BHs). We should mention that these Monte Carlo models assumed that BHs and neutron stars received the same (large) natal kicks, naturally leading to a small number of retained BHs early on. Our constraints on the BH content in 47 Tuc are also in keeping with the low number of retained BHs implied by the results of Askar et al. (2018) and Arca Sedda et al. (2018) and in agreement with the population of \( \sim 20 \) BHs (but possibly as large as \( \sim 150 \) BHs within \( 2r_c \)) inferred by Weatherford et al. (2018) based on the observed mass segregation between giants and main-sequence stars in the central regions of the cluster, although we note that our models are simultaneously fitted to several additional observables. To model the velocity dispersion in the core of 47 Tuc with the main goal of placing constraints on the presence of an IMBH, Mann et al. (2019) took into consideration populations of objects more centrally concentrated than the typical main-sequence stars (binaries and stellar remnants) which may cause the velocity dispersion to rise in the core and affect the inferred IMBH mass. They found that concentrated populations of binary stars and dark stellar remnants alone appear to be enough to explain the velocity dispersion in the core, and thus that there is no evidence for an IMBH (unless an unrealistically small population of remnants is assumed). Pushing their adopted retention of neutron stars and BHs higher than \( \sim 8.5\% \) even led to a larger velocity dispersion than is observed in the core, requiring an unphysical negative IMBH mass in their Jeans model fit. Given their assumptions about the initial BH population and their adopted object mass of \( 10 \, M_\odot \) for each BH, this maximum retention fraction translates to an upper limit of 1615 \( M_\odot \) in BHs, consistent with our new constraints. All these results are in keeping with the presence of a strong BH binary candidate in 47 Tuc (X 9; Miller-Jones et al. 2015; Bahramian et al. 2017; Church et al. 2017; Tudor et al. 2018), consistent with the idea that 47 Tuc still hosts at least some BHs today.

Forcing our models to retain a significantly larger population of BHs would adversely affect the quality of the fit by producing a core that is too large and suppressing mass segregation to the extent that the observed change in the local stellar mass function slope with radius cannot be matched. As most BHs formed in 47 Tuc are expected to have been ejected dynamically (see below), the inferred upper limit provides important constraints on the dynamical evolution history of the cluster.

Due to our adopted prescription for the initial-final mass relation of massive stars, our assumption that the more massive black holes are ejected first, and the low inferred low dynamical retention fraction of BHs, the present-day population of BHs that we infer in 47 Tuc is comprised of objects of a few solar masses only and at most \( \sim 6 \, M_\odot \) (see Fig. 7). If the retained BHs were in reality more massive on average, our reported number of retained BHs would overestimate the true number of BHs and should then be taken as an upper limit (if the BHs are more massive, fewer are needed to produce the same dynamical effect). This would be the case if a significant mass gap exists between the heaviest neutron stars and the lightest BHs (with no BH below \( \sim 5 \, M_\odot \), e.g. Belczynski et al. 2012), which is not captured in our adopted initial-final mass relation (our minimum BH mass is 2.6 \( M_\odot \)).

Our assumption that the massive BHs are preferentially removed (as expected from dynamical ejections) could possibly also lead to a similar bias. A fraction of the BHs formed in a GC is expected to leave the cluster due to experiencing natal kicks larger than the escape velocity at the time of supernova. This is expected to lead to a mass-dependent retention fraction and predominantly remove low-mass BHs. However, the present-day central escape velocity of our model is \( \gtrsim 50 \, \text{km} \, \text{s}^{-1} \) and this would have been at least a factor of two higher at birth because of stellar mass loss and subsequent adiabatic expansion. If we assume that BHs receive the same momentum kick as neutron stars, then Antonini & Gieles (2019) showed that for escape velocities above \( \sim 100 \, \text{km} \, \text{s}^{-1} \) almost all BHs are retained (their Fig. 1). Note however that according to the mass fallback prescription, low-mass BHs will receive larger natal kicks and it would be easier for them to escape the system. The argument above about the escape velocity might be softened because initial mass loss associated with the most massive stars will lower the central potential before lower-mass BHs form. This would lead to a larger average BH mass at the present day. On the other hand, the initial escape velocity could have been substantially higher than the conservative estimate obtained from correcting for adiabatic expansion only, as we will discuss in Section 5.3.

An exciting prospect to break the degeneracy between dynamically ejected BHs and those lost via natal kicks is by finding BH candidates with reliable mass estimates, either with multi-epoch spectroscopy if they are in a detached binary with a stellar companion (Giesers et al. 2018), or microlensing of background (SMC) stars or quasars (Wyrzykowski et al. 2016; Wyrzykowski & Mandel 2019). This would provide constraints on the BH mass function in our mass models and therefore on natal kicks and dynamical BH ejection, because a small dynamical retention fraction implies low BH masses, while a small retention fraction resulting from natal kicks leads to a high BH masses (if natal kicks are larger for low-mass BHs).

### 5.1.3 The effect of binaries

We did not explicitly include binary systems when building the global present-day mass function for our multimass models, and it is worth discussing the potential effect of ignoring these binaries. From an analysis on the visual/near-infrared colour-magnitude diagram (CMD) of 47 Tuc stars, Mann et al. (2019) estimated binary fractions in different mass-ratio \((q)\) ranges (above \( q = 0.5 \), where binaries can be isolated from the single-star main sequence). For the ranges, \( 0.5 < q < 0.7, 0.7 < q < 0.9, \) and \( q > 0.9, \) they find binary fractions of 2.65%, 0.98%, and 0.3%, respectively.

Only binaries with a primary mass close to the main-sequence turnover mass and a \( q \) above \( \sim 0.7 \) would have a system mass comparable to neutron stars. From the estimates in Table 2 of Mann et al. (2019), the binaries with a system mass above \( 1.4 \, M_\odot \) could make up to \( \sim 5000 \, M_\odot \) of the cluster mass. This is less than 1% of the total cluster mass but these objects would be concentrated in the inner regions of the cluster due to mass segregation and could provide a significant contribution to the gravitational potential there. However, in our tests where we changed the adopted retention fraction of neutron stars, we found that retaining anywhere from very few to several thousands of neutron stars did not significantly affect our results, in particular with respect to the mass in BHs and IMF. Neutron stars (and heavy binaries with comparable mass) are
thus expected to be relatively unimportant dynamically. Their total mass contribution would actually be dwarfed by the mass in massive (> 1 M⊙) white dwarfs in our best-fitting model, which add up to ~ 6 × 10^6 M⊙.

Interestingly, from their CMD analysis, Mann et al. (2019) estimate a total mass of ~ 41,500 M⊙ in heavy binaries (> 1 M⊙), and their assumptions about the mass function and retention of stellar remnants lead to a mass of ~ 27,600 M⊙ in heavy remnants (massive white dwarfs > 1 M⊙, neutron stars, BHs) in their model. Their total mass in objects more massive than 1 M⊙ (~ 6.9 × 10^4 M⊙) is therefore very comparable to what we infer in our multimass model. By ignoring heavy binaries when building our multimass model, there is therefore a possibility that this missing mass is compensated by favouring more mass in heavy remnants and a model with a high-mass IMF (α) that is shallower than the true cluster IMF. In that respect, it is interesting to recall that the Monte Carlo model of 47 Tuc by Giersz & Heggie (2011) required a relatively steep IMF for stars above the main-sequence turnover, with an index of about 2.8 (compared to 2.35 for a Salpeter mass function), but still a relatively flat IMF for the lower main sequence (α = 0.4).

The vast majority of (undetected) low-q binaries (q < 0.5) would have total binary masses below 1 M⊙ and behave dynamically like the general main-sequence population, but they could potentially bias the star counts as a function of mass in the observed local stellar mass functions. However, even under the conservative assumption than only a quarter of binaries have q > 0.5, the total binary fraction is expected to be < 10% in 47 Tuc (e.g. Milone et al. 2012) and we do not expect this small population of low-q binaries to affect our conclusions. We defer a detailed treatment of the effect of binaries on our models to future work.

We note that Mann et al. (2019) inferred a total cluster mass and a central velocity dispersion that are significantly larger than what other studies have found for 47 Tuc, and this may have led them to overestimate the total mass in binaries and in heavy remnants. They obtain a total cluster mass of 1.47 × 10^6 M⊙, at least ~ 35% higher than what we (Table 1), Giersz & Heggie (2011), and Baumgardt & Hilker (2018) found. This could partly be due to a limitation of their method, which only fits on kinematic data in the central region of the cluster and does not yield a self-consistent model of different observables (e.g. not including the density distribution) over the whole spatial extent of the cluster. Their central velocity dispersion (~ 14 – 15 km s⁻¹) is also high compared to the value of ~ 12 km s⁻¹ that is derived from the LOS velocities and that we find from our fit to the the proper motion and line-of-sight kinematic data of Baumgardt & Hilker (2018) and Watkins et al. (2015). It is not clear what the range of magnitudes (and corresponding masses) of the stars entering the central velocity dispersion profile of Mann et al. (2019) is, but if stars fainter than the main-sequence turnover (thus lower-mass tracers) were included, it may explain the discrepancy; the kinematic data that we used are based on samples of stars with a mass comparable to turnover stars. An indication in that sense comes from the central proper motion velocity dispersion measured by McLaughlin et al. (2006) for stars with a mass comparable to the turnover mass, 0.609±0.010 mas yr⁻¹, which corresponds to 12.8 km s⁻¹ when scaled to a distance of 4.45 kpc, significantly lower than the value of ~ 14 – 15 km s⁻¹ reported by Mann et al. (2019).

5.2 The initial stellar mass function

We have seen in the previous section that the global stellar mass function of 47 Tuc is significantly shallower at low masses than that of a ‘canonical’ (Kroupa 2001) IMF. Because of the long half-mass relaxation time of 47 Tuc (log(t/h/yr) = 9.7), and its relatively circular orbit (Gaia Collaboration et al. 2018), it is unlikely that the long-term preferential escape of low-mass stars as the result of equipartition has played an important role. Given our current knowledge of the cluster’s orbit, 47 Tuc is not expected to have lost a significant amount of its initial mass (beyond mass loss from stellar evolution; e.g. Balbinot & Gieles 2018). In fact, dynamical Monte Carlo of models of 47 Tuc require a flat (low-mass) IMF as initial conditions to reproduce a flat present-day mass function (Giersz & Heggie 2011). Other GCs with similar t_h tend to have steeper low-mass mass functions (corresponding to α indices of ~ 1, Sollima & Baumgardt 2017; their figure 3), making 47 Tuc a clear outlier. Fig. 7 illustrates the inferred present-day global mass function of stars and remnants from our best-fitting multimass model of 47 Tuc, along with the corresponding initial mass function.

From integrated light studies of GCs in M31 and the Milky Way, Strader et al. (2011) and Kimmig et al. (2015) found an anti-correlation between the V-band mass-to-light ratio (V/T_V) and metallicity ([Fe/H]). Because SSP models predict a correlation between T_V and [Fe/H], these findings can be interpreted as metal-rich GCs having bottom-light MFs (i.e. fewer dwarfs) and/or top-light MFs (i.e. fewer remnants). However, light-weighted velocity dispersions and half-light radii of mass segregated clusters are sensitive to [Fe/H] dependent biases (Sippel et al. 2012), which can give rise to
the observed anti-correlation between the dynamical $\tau_V$ and [Fe/H] even if all GCs formed with the same canonical IMF (Shanahan & Gieles 2015). The latter authors also showed that the dynamically inferred $\tau_V$ for a canonical MF is similar to that of a bottom-light MF, making $\tau_V$ a particularly poor proxy of the MF at low masses in mass segregated GCs.

Hence resolved GCs are needed to make a solid statement about the MF slope at high [Fe/H]. 47 Tuc is among the most metal-rich Milky Way GCs at a relatively close distance for which kinematics and star counts are available. Our findings suggest that indeed the IMF of this cluster could have been both bottom light and (somewhat) top light compared to the canonical IMF. The universality of the IMF is an ongoing debate, and it can not be concluded yet whether 47 Tuc is a genuine threat to the universality hypothesis or can be reconciled with other GCs once scatter in the outcome of IMF sampling is considered. But it is interesting to note that a putative correlation between MF slope index and [Fe/H] is opposite of what is found in extragalactic studies of early-type galaxies. Systematically larger $\tau_V$ have been reported in more massive (i.e. more metal-rich) early-type galaxies based on dwarf-sensitive spectral features (e.g. Conroy & van Dokkum 2012), kinematics (e.g. Cappellari et al. 2012) and strong lensing (e.g. Treu et al. 2010).

A spectral analysis of (integrated-light properties of) 47 Tuc (as in Villaume et al. 2017), similar to what is done for early-type galaxies, would be an interesting step towards understanding this potentially troubling contradiction between IMF variations in GCs and early-type galaxies.

5.3 Black holes, the IMF, and the early dynamical evolution of 47 Tuc

There is an important caveat to the argument above about a possible bottom-light IMF for 47 Tuc. Even though it is unlikely that the cluster suffered significant preferential escape of low-mass stars during its long-term evolution (given its long half-mass relaxation time and orbit), there remains a possibility that the loss of low-mass stars occurred early on. If 47 Tuc formed with a high enough density, it could have become completely mass segregated (and thus vulnerable to the loss of low-mass) on a short timescale (an extreme initial half-mass density of $10^4 M_\odot/pc^3$ would imply an initial half-mass relaxation time of $\sim 100$ Myr).

While tides at the present-day orbit are too weak to remove low-mass stars, tidal perturbations with giant molecular clouds (GMCs) during the early evolution could have played a role, although for a large initial density the timescale for this process would also be very large. It also remains to be seen whether this can lead to a change in the low-mass mass function by $\Delta \alpha \approx 0.8$ and explain the inferred present-day mass function with a standard IMF. From Baumgardt & Makino (2003), a cluster needs to lose about 85% of its initial mass by evaporation to achieve $\alpha \approx 0.8$. About 45% of this mass loss is due to stellar evolution, so the cluster needs to lose about 40% of its initial mass through evaporation. For a present day mass of $\sim 1 \times 10^6 M_\odot$, this implies an initial mass of $\sim 6.7 \times 10^5 M_\odot$. However, we need to be cautious with using this relation between mass loss and $\Delta \alpha$ to other mass loss mechanisms, because the way low-mass stars are lost could be different.

For example, tidal perturbations remove stars at large radii, while evaporation removes stars with high energies, and this may not lead to the same $\Delta \alpha$ for a given amount of mass loss.

Interestingly, a very high initial density might explain why 47 Tuc has retained almost no BHs, which is otherwise puzzling given its relatively long relaxation time and large radius (see e.g. Breen & Heggie 2013). Dense initial conditions are needed to dynamically eject most BHs during a Hubble time. The Monte Carlo model of 47 Tuc by Giersz & Heggie (2011) has an initial half-mass density of $\sim 3 \times 10^4 M_\odot/pc^3$, but we recall that in their models the BHs received the same (large) natal velocity kicks as the neutron stars. Using the fast cluster evolution model of Antonini & Gieles (2019) and assuming that the BHs receive the same momentum kick as the neutron stars, we find that an initial density of $\sim 10^6 M_\odot/pc^3$ is required to dynamically eject nearly all BHs (assuming an initial mass in BHs of 4% of the total initial mass, appropriate for the metallicity of 47 Tuc). Although speculative, it could be that more metal-rich GCs like 47 Tuc form substantially denser (due to more efficient cooling) and fully segregate soon after formation, which leads to a flattening of their mass function by various disruption processes like interactions with GMCs. A potential complication is that the high initial density required to quickly mass segregate the cluster and dynamically eject the BHs makes the cluster more resilient to tidal perturbations and makes it harder to reach the present-day $r_h \approx 8$ pc. In future modelling efforts, understanding the interplay between the evolution of the cluster size, black hole population, and mass function will be key to understand the IMF of 47 Tuc and the evolution of its BH population.

6 CONCLUSIONS

We presented a self-consistent multimass LMPV model of 47 Tuc where the mass function and content of stellar remnants were free to vary and constrained by finding the best simultaneous match to a range of observational constraints: number density profile, kinematics (line-of-sight and proper motion dispersion profiles), and stellar mass function at different projected distances from the cluster centre. Not only does our best-fitting model satisfactorily match all these observations, it also correctly predicts the radial distribution of MSPs in 47 Tuc and can accommodate the line-of-sight accelerations of MSPs inferred from their period derivatives. Our main findings can be summarized as follows:

- There is no need for an IMBH in 47 Tuc given the current data. Our model, which does not include an IMBH, can successfully explain a range of observables including the line-of-sight accelerations (or upper limits on these) of MSPs. We thus concur with the conclusions of Mann et al. (2019) rebutting the findings of Kızıltan et al. (2017).
- We constrain the stellar-mass BH population in 47 Tuc to contain a total mass of $4.3 \times 10^3 M_\odot$, or equivalently $141^{+67}_{-57}$ BHs (for a mean BH mass of 3.1 $M_\odot$). This serves as a demonstration of the power of the mass modelling technique presented here to address questions about the BH content of GCs by modelling their present-day properties. These results also provide important constraints on the dynamical evolution history of 47 Tuc and its BH population.
- We infer a relatively shallow present-day global stellar MF and IMF for 47 Tuc ($\alpha_1 = 0.52^{+0.17}_{-0.16}$ and $\alpha_2 = 1.35^{+0.25}_{-0.23}$ compared to the steeper values of $\alpha_1 = 1.3$ and $\alpha_2 = 2.3$ for a Kroupa IMF), in keeping with previous results from evolutionary dynamical models of this cluster (e.g. Giersz & Heggie 2011). Given our current
knowledge of the orbit and predictions for the long-term mass-loss history of 47 Tuc, it is not expected to have lost a significant amount of its initial mass (beyond mass loss from stellar evolution), and preferential loss of low-mass stars due to long-term dynamical evolution in the tidal field of the Milky Way should have been minimal. The shallow global present-day mass function inferred for main-sequence stars therefore hints at a possible dearth of low-mass stars and a bottom-light IMF. However, we cannot exclude that a loss of low-mass stars occurred early on in the evolution of 47 Tuc. Interestingly, the high initial density that would be required in this case may be linked to the fact that the cluster has retained almost no BHs despite its relatively long relaxation time and large radius at the present day. We emphasize that understanding the interplay between the evolution of the cluster size, black hole population, and mass function will be key to understand the IMF of 47 Tuc and the evolution of its BH population.

- At higher masses, our inferred IMF slope is close to Salpeter (\(\alpha_1 = -2.49 \pm 0.08\) compared to \(\alpha = 2.35\) for Salpeter), although this slope might be steeper if we included the contribution of heavy binaries. In any case, the method presented here, which relies on modelling the dynamical effect of otherwise unseen dark remnants (mainly white dwarfs), provides a promising new way to probe the IMF at high masses in GCs and to address questions about possible variations with environment.

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**On the black hole content and IMF of 47 Tuc**

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