Gate control of the spin mobility through the modification of the spin-orbit interaction in two-dimensional systems

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Spin drag measurements were performed in a two-dimensional electron system set close to the crossed spin helix regime and coupled by strong intersubband scattering. In a sample with unexplored opportunities for the study of spin transport, the drift transport allows us to determine the spin-orbit field and the spin mobility anisotropies. We used a random walk model to describe the system dynamics and found excellent agreement for the Rashba and Dresselhaus couplings. The proposed two-subband system displays a large tuning lever arm for the Rashba constant with gate voltage, which provides a new path towards a spin transistor. Furthermore, the data shows large spin mobility controlled by the spin-orbit constants setting the field along the direction perpendicular to the drift velocity. This work directly reveals the resistance experienced in the transport of a spin-polarized packet as a function of the strength of anisotropic spin-orbit fields.

The pursuit for a new active electronic component based on flow of spin, rather than that of charge, strongly motivates research in semiconductor spintronics [1–5]. Since the Datta-Das proposal for a ballistic spin transistor, full electrical control of the spin state was suggested using the gate-tunable Rashba spin-orbit interaction (SOI) [6–10]. Further studies, including the Dresselhaus SOI [11], were made to assure a nonballistic transistor robust against spin-independent scattering [12–14]. For example, it has been demonstrated that SU(2) spin rotation symmetry, preserving the spin polarization, can be obtained in the persistent spin helix (PSH) formed when the strengths of the Rashba and Dresselhaus SOI are equal ($\alpha = \beta$) [15–19]. This is possible because the uniaxial alignment of the spin-orbit field suppresses the relaxation mechanism when the spins precess about this field while experiencing momentum scattering [20]. Gate control of this symmetry point was experimentally observed [21–23] and allowed to produce a transition to the PSH ($\alpha = -\beta$) in the same subband [24]. Drift in those systems showed surprising properties [25, 26] such as the current-control of the temporal spin-precession frequency [27]. Although the helical spin-density texture could be even transported without dissipation under certain conditions [15], the spin transport suffers additional resistance from the spin Coulomb drag [28–32]. These frictional forces appear as a lower mobility for spins than for charge and studies in new systems are still necessary to understand this important constraint for future devices.

A two-dimensional electron gas (2DEG) hosted in a quantum well (QW) with two occupied subbands offers unexplored opportunities for the study of spin transport [33, 34]. Theoretically, the inter- and intra-subband spin-orbit couplings (SOCs) have been extensively studied [35–38]. In terms of a random walk model (RWM) [39], the spin drift and diffusion was recently developed for these systems displaying two possible scenarios regarding the intersubband scattering (ISS) rate [40]. The interplay between the two subbands may introduce new features to the PSH dynamics, for example, a crossed persistent spin helix [41] may arise when the subbands are set to orthogonal PSHs (i.e., $\alpha_1 = \beta_1$ and $\alpha_2 = -\beta_2$) in the weak ISS limit. In this report, we experimentally study spin drag in a system with the two subbands individually set close to the PSH$^+$ and PSH$^-$, but with strong ISS, where the dynamics is given by the averaged SOCs of both subbands. The combination of long spin lifetime and high charge mobility allows us to determine the spin mobility and the spin-orbit field anisotropies with the application of an accelerating in-plane voltage. We are able to control the SOCs in both subbands and to show a linear dependence for the sum of the Rashba constants with gate voltage. Finally, we determine an inverse relation for the spin mobility dependence on the SOCs directly revealing the resistance experienced in the transport of a spin-polarized packet as a function of the strength of anisotropic spin-orbit fields.

The sample consists of a single 45 nm wide GaAs QW grown in the [001] (z) direction and symmetrically doped. Due to the Coulomb repulsion of the electrons, the charge distribution experiences a soft barrier inside the well. Figure 1(a) shows the calculated QW band profile and charge density for both subbands. The electronic system has a configuration with symmetric and antisymmetric wave functions for the two lowest subbands with subband separation of $\Delta_{SAS} = 2$ meV. The subband density ($n_1 = 3.7, n_2 = 3.3 \times 10^{11}$ cm$^{-2}$) was obtained from the Shubnikov-de Hass (SdH) oscillations as shown in...
Fig. 1(a) and the low-temperature charge mobility was $2.2 \times 10^6$ cm$^2$/Vs [42]. A device was fabricated in a cross-shaped configuration with width of $w = 270$ µm and channels along the [110] (x) and [110] (y) directions. Lateral Ohmic contacts deposited $l = 500$ µm apart were used to apply an in-plane voltage ($V_{ip}$) in order to induce drift transport. For the fine tuning of the subband SOCs, a semitransparent contact on top of the mesa structure ($V_g$) was used to modify structural symmetry and subband occupation. The effect of $V_g$ on the subband energy levels ($\epsilon_{\nu}$) and densities ($n_{\nu}$) is shown in Fig. 1(b) and (c) as a function of the out-of-plane electric field ($E_z$). Note that the total density changes linearly with $V_g$ and that $V_g = 0$ corresponds to a built-in electric field of 0.15 V/µm. Figure 1(d) displays the experimental scheme with the connection of $V_{ip}$ and $V_g$ [43].

To describe the magnetization dynamics and the measured SO fields for our two-subband system, we combine the calculated SOCs with RWM [39, 40, 44]. For a [001] GaAs 2DEG, the x and y components of the SO fields for each subband $\nu = \{1, 2\}$ are

$$B_{SO, \nu}(k) = \frac{2}{g\mu_B} \left( + \alpha_\nu + \beta_1\nu + 2\beta_3\nu \frac{k_x^2 - k_y^2}{k_x^2 + k_y^2} k_y \right)$$

$$\left( - \alpha_\nu + \beta_1\nu - 2\beta_3\nu \frac{k_x^2 - k_y^2}{k_x^2 + k_y^2} k_x \right),$$

(1)

plus corrections due to the intersubband SOCs [23, 35–38, 41]. Above, $g = -0.44$ is the electron g-factor for GaAs and $\mu_B$ is the Bohr magneton. The SOCs are the usual Rashba $\alpha_\nu$ and linear $\beta_1\nu$ and cubic $\beta_3\nu$ Dresselhaus terms. Considering the strong intersubband scattering (ISS) regime of the RWM [40], the randomization of the momenta $k$ (within the Fermi circle $k = k_F$) and subband $\nu$ is much faster than the spin precession. Consequently, the dynamics is governed by an averaged SOC field $\langle B_{SO} \rangle = \langle (B_{SO}^x, B_{SO}^y) \rangle$ transverse to the drift velocity $v_{dr} = (v_{dr}^x, v_{dr}^y)$. Namely, the field components read

$$\langle B_{SO}^x \rangle = \left[ \frac{m}{\hbar g \mu_B} \sum_{\nu=1}^{2} (+\alpha_\nu + \beta_1^\nu) \right] v_{dr}^y,$$

(2)

$$\langle B_{SO}^y \rangle = \left[ \frac{m}{\hbar g \mu_B} \sum_{\nu=1}^{2} (-\alpha_\nu + \beta_1^\nu) \right] v_{dr}^x,$$

(3)

where $\beta_1^\nu = \beta_1\nu - 2\beta_3\nu$, and $m = 0.067m_0$ is the effective electron mass for GaAs and $\hbar$ is Planck’s constant. Since $B_{SO}^x \propto v_{dr}^y$ and $B_{SO}^y \propto v_{dr}^x$, it is convenient to analyze the linear coefficients $b^x(y) = B_{SO}^x / v_{dr}^y$, which are given by the
The intra- and intersubband SOCs are calculated within the self-consistent Hartree approximation [35–38] for GaAs quantum wells tilted by $E_z$. The chemical potential is set to return the density $n = n_1 + n_2 = 7 \times 10^{11}$ cm$^{-2}$ for $E_z = 0$, while it varies linearly for finite $E_z$ in Fig. 1(c). The SOCs are defined from the matrix elements $\eta_{\nu,\nu'} = \langle \nu | \eta_{x} V' + \eta_{y} V_H' | \nu' \rangle$ and $\Gamma_{\nu,\nu'} = \gamma \langle \nu | k_z^2 | \nu' \rangle$, where $| \nu \rangle$ is the eigenket for subband $\nu$, $\eta_{x} = 3.47$ Å$^2$ and $\eta_{y} = 5.28$ Å$^2$ are bulk coefficients [35–38, 45], $V' = \partial_z V(z)$ and $V_H' = \partial_z V_H(z)$ are the derivatives of the heterostructure and Hartree potentials along $z$, $\gamma = 11$ eV Å$^{-1}$ is the bulk Dresselhaus constant, and $k_z$ is the $z$-component of the momentum. The usual intra-subband Rashba and linear Dresselhaus SOCs are $\alpha_{\nu} = \eta_{\nu,\nu}$ and $\beta_{1,\nu} = \Gamma_{\nu,\nu}$. The non-diagonal terms are the intersubband SOCs $\eta = \eta_{12}$ and $\Gamma = \Gamma_{12}$. The calculated SOCs, plotted in Fig. 2(a)-(c) as a function of $E_z$, show agreement with previous studies [46, 47]. The high-density $n$ makes the cubic Dresselhaus $\beta_{1,\nu} \approx \gamma \eta_{\nu,\nu}/2$ comparable with $\beta_{1,\nu}$, strongly affecting the PSH tuning [17] $\alpha_{\nu} = \beta_{\nu}$, with $\beta_{\nu} = \beta_{1,\nu} - \beta_{\nu}$.

Near $E_z \approx 0.04$ V/µm, the SOCs reach almost simultaneously the balanced condition for the PSH$^+$ in the first subband ($\alpha_1/\beta_1 = +1$) and for the PSH$^-$ in the second subband ($\alpha_2/\beta_2 = -1$), as shown by the ratio $\alpha_{\nu}/\beta_{\nu}$ in Fig. 2(d). The expected magnetization patterns for the single-subband PSH is shown in the inset of Fig. 2(d). The PSH$^-$ shows more stripes than the PSH$^+$ due to the higher value of $\alpha$, which grows quickly within the $E_z$ range. However, the ratio of the averaged SOCs $(\sum \alpha_{\nu})/(\sum \beta_{\nu})$ approaches the PSH regimes only for $|E_z| > 0.3$ V/µm. As we will see next, the experimental data matches well the strong ISS regime of the RWM, therefore the dynamics is governed by the averaged SOCs. In this case, the expected magnetization patterns are shown in Fig. 2(e). With increasing $E_z$ the system transitions from isotropic ($E_z = 0$) to uniaxial ($E_z > 0.3$ V/µm), as indicated by the formation of stripes and the orientation of the first harmonic component of the total field $\sum B_{SO,\nu}(k)$ [arrows in Fig. 2(e)].

We are interested in the determination of the anisotropy for the coefficients $b^{(i)}(y)$, estimated in one order of magnitude in Fig. 3(a) and (b). We measured the spin polarization using time-resolved Kerr rotation as function of the space and time separation of pump and probe beams. All optical measurements were performed at 10 K. A mode-locked Ti:Sapphire laser with a repetition rate of 76 MHz tuned to 816.73 nm was split into pump and probe pulses. The polarization of the pump beam was controlled by a photelastic modulator and the intensity of the probe beam was modulated by an optical chopper for cascaded lock-in detection. An electromagnet was used to apply an external magnetic field in the plane of the QW. The spatial positioning of the pump relative to the probe (d) was controlled using a scanning mirror. We defined the spin injection point to be $x = y = 0$ at $t = 0$. The application of an in-plane electric field $(E_{ip} = V_{ip}/l)$, in the $x$ or $y$-oriented channel, adds a drift velocity to the 2DEG electrons and allows us to determine the spin mobility and the spin-orbit field components [48–50].

The sample was rotated such that each channel under study was oriented parallel to the external magnetic field $B_{ext} \parallel |v_{dr}|$ for all measurements reported here. From the SOI form in k-space, we expected $B_{SO} \perp v_{dr}$ implying that the observable $B_{SO}$ direction will be $B_{SO} \perp B_{ext}$. Considering this orientation, we can model the Kerr rotation signal as $\phi_K(B_{ext}, d) = \Lambda(d) \cos(\omega t)$ with the precession frequency $\omega = (g\mu_B/eh)^{1/2} B_{ext}^2 + B_{SO}^2$, where $\Lambda(d)$ is the amplitude at a given pump-probe spatial separation and $B_{SO}$ is the internal SO field component perpendicular to $B_{ext}$ (and to $v_{dr}$).

Figure 3 shows the results of the spin drag experiment with the gate contact open. Scanning the pump-probe separation in space at fixed long time delay (13 ns), we determined the central position $d_c$ of the spin packet
amplitude for several $V_{ip}$ in a given crystal orientation. From the values of $d_c$ in Fig. 3(c), we calculated the drift velocity as $v_{dr}=d_c/t$ and plotted it as a function of $V_{ip}$ in Fig. 3(d). The slope of the linear fit gives us spin mobilities ($\mu_{s}^{x,y}$) in the range of $10^5$ cm$^2$/Vs. Values in the same order of magnitude have been measured by Doppler velocimetry for the transport in single subband samples [32]. Nevertheless, in those systems the spin lifetimes were restricted to the picosecond range and the transport was limited to the nanometer scale.

Following the drifting spin packet in space, Fig. 3(e) displays a $B_{ext}$ scan from where changes in the amplitude of zeroth resonance determined $B_{SO}$ strength at $d_c$. As explained above, the data confirmed the perpendicular orientation between $B_{SO}$ and $v_{dr}$ and did not show a component parallel to $B_{ext}$ within the experimental resolution [51]. From the Lorenzian shape of the $B_{ext}$ scan [52, 53], we evaluated a spin lifetime of 7 ns at $V_{ip}=0$. This experiment was only possible due to the nanosecond spin lifetime in our sample that extends the spin transport to several tens of micrometers [54, 55].

Figure 3(f) shows the fitted values of $B_{SO}$ for several $V_{ip}$ applied along x and y. We observed highly anisotropic spin-orbit fields in the range of several mT as expected from Fig 3(a) and (b). The $B_{SO}$ orientation was aligned primarily with the x axis in agreement with the simulation in Fig 2(e). The slopes $b^x(y)=B_{SO}^{x(y)}/v_{dr}^{x(y)}$ give the strength of the SOCs that generate the field according to Eqs. 2 and 3. For this condition of the sample as-grown, we found $\sum \alpha_v = 0.57$ meVÅ and $\sum \beta_v = 0.75$ meVÅ.

Note the inverse behaviour on $V_{ip}$ for the mobility and for $B_{SO}$ strength in perpendicular directions. In Fig. 3(c) and (d), the axis with the largest mobility is also the axis with smaller spin-orbit field in the perpendicular direction. This result may be related to the spin Coulomb drag observed previously in the transport of spin-polarized electrons [31, 32]. Next, we demonstrate the direct control of the spin mobility through the gate modification of the subband SOCs.

Figure 4(a) shows that the magnitude and the orientation with the largest $\mu_s$ can be tuned by $E_z$. $B_{SO}$ displays anisotropic components with $B_{SO}^x$ being larger in all the studied range, which confirms the preferential alignment towards the PSH+ in Fig. 2(e). The variation of $B_{SO}^x$ has a minimum (indicated by an arrow) close to position when the second subband attains the PSH− (with $B_{SO}$ along y). Dividing Fig. 4(a) panels, the values for b are plotted in Fig. 4(b). The lines plotted together with the data are the expected values using Eq. 2 and 3 with the SOCs from Fig. 2(a)-(c). When the QW approaches the symmetric condition ($E_z=0$), $b^x(y)$ decreases removing the anisotropy of $B_{SO}$ as simulated in Fig. 2(e).

The addition and subtraction of $b^x$ and $b^y$ give the sum of the Rashba and Dresselhaus SOCs displayed in Fig. 4(c). Dashed lines corresponding to the purple curves in Fig.2(a) and (c) are plotted together displaying excellent agreement. The slope for the Rashba SOI indicates a tuning lever arm of 35 eA$^2$. This value is considerably larger than those reported in recent studies for single subband samples, typically below 10 eA$^2$ [17, 23]. Finally, Fig. 4(d) presents $\mu_{s}^{x(y)}$ [from (a)] against the SOCs defining $B_{SO}^{y(x)}$: $\sum(-\alpha_v + \beta_v)$ and $\sum(\alpha_v + \beta_v)$, respectively. This last plot illustrates the inverse dependence, with negative slope, for the spin mobility and strength of the SOCs perpendicular to the drift direction. The different slopes for x and y channels give us a hint that this effect depends not only on how $B_{SO}$ changes with $v_{dr}$ (given by the SOCs) but also in the magnitude of the fields. A common maximum value $\mu_{s}^0=3\times10^5$cm$^2$/Vs was found independent of $v_{dr}$ orientation.

In conclusion, we have studied a 2DEG system with two subbands set close to the crossed PSH regime under strong intersubband scattering and successfully described it using a random walk model. In the spin transport with nanosecond lifetimes over micrometer distances, we demonstrate the control of the subbands spin-orbit couplings with gate voltage and observed spin mobilities in the range of $10^5$cm$^2$/Vs. Specifically, the sum of the Rashba SOCs presents a linear behaviour with remarkably large tunability lever arm with gate voltage. We
tailored the spin mobility by controlling the strength of the spin-orbit interaction in the direction perpendicular to the drift velocity. Our findings provided evidence of the rich physical phenomena behind multiband systems and experimentally demonstrated relevant properties required for the implementation of a nonballistic spin transistor.

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