Antlion Optimized Robust Control Approach for Micropositioning Trajectory Tracking Tasks

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This work was supported in part by the Australian Research Council (ARC) Linkage Infrastructure, Equipment and Facilities (LIEF) grant and in part by the ARC Discovery grant.

ABSTRACT Planar 3-Degree of Freedom (3-DOF) micropositioning stages are widely adopted in many precision applications for their ability to provide in-plane rotation. However, their motion accuracy is adversely affected by cross-couplings, model uncertainty, and external disturbances. This work proposes an optimized robust control methodology based on disturbance estimation to address these issues. Systematic modeling of a 3-DOF precision micropositioning stage was utilized to develop a nonlinear disturbance observer-based sliding mode control methodology. This methodology can estimate and compensate the unavoidable cross-couplings between the major axes of motion. A stability analysis is conducted to prove the stability of the feedback system when the control approach is combined with the disturbance observer. A maximum bound on the tracking error is derived through finite-time analysis, and the parameters that affect this bound are identified. The antlion optimizer algorithm is used to optimize the control parameter based on the mean square error cost function to eliminate the requirement for manual tuning and to achieve the best attainable performance. The proposed control method is experimentally demonstrated to track complex trajectory with less tracking error than the classical sliding mode approach. The main contribution of this study is the improvement of the trajectory tracking accuracy in multi-DOF micropositioners using an optimized disturbance observer-based robust control technique.

INDEX TERMS Sliding mode, disturbance observer, metaheuristic optimization, antlion optimizer, micropositioning.

I. INTRODUCTION Planar Three Degree of Freedom (3-DOF) micro/nanopositioning mechanisms are essential in fields requiring both translation and orientation correction. Orientation correction is necessary to align samples with apparatus in processes such as photolithography, manipulation under atomic force microscope, micro-assembly, and many more \([1]–[3]\). Compliant mechanisms (CM) are typically used in the design of micro/nanopositioning mechanisms as they offer several advantages such as monolithic configuration, compact structure, high precision, zero backlash, and no wear \([4]–[6]\). Compliant manipulators are designed such that flexible elements’ deformation transforms loads into motions \([7]\).

XY micromanipulators are another planar type mechanisms which have been extensively studied in the literature as they offer an extensive range of motion; a few examples can be referred to \([8]–[11]\). Improving rotational stiffness and the utilization of decoupling mechanisms are usually employed in those mechanisms to improve the motion range and reduce parasitic motions such as cross-coupling and in-plane rotation. Despite the popularity of decoupling mechanisms that are used within XY micropositioners, in practice, cross-coupling and in-plane rotation still occur in linear
motions due to assembly and manufacturing errors. These induced errors severely degrade motion accuracy, and thus a rotational compensation is required. The extra DOF offered by the planar 3-DOF micro/nanopositioning mechanisms can easily be used for orientation correction and manipulation to overcome these issues [12].

Planar 3-DOF XYθ mechanisms have coupled kinematics, which makes them inherently more challenging to control than the decoupled XY mechanisms. The strongly present cross-axis coupling in these mechanisms has a substantial impact on the positioning accuracy. Moreover, it can even cause actuator damage if it was large enough [13]. The adverse effect of coupling is not only limited to flexure-based mechanisms; it was found that it results in mechanical components damage and excessive wear in sliding parts in dual-driven gantry systems. This behaviour was investigated and resolved by synchronizing the motors motions using advanced synchronization control schemes proposed in [14], and [15]. In flexure-based mechanisms, several attempts were directed towards improving the mechanical design to tackle the cross-coupling issues. Serial kinematics was considered in [16] where the θ-axis was serially connected to a decoupled XY stage. Although this configuration decouples the axes and simplifies its control, it could result in nonhomogeneous dynamics. Moreover, the cascaded structure results in large inertia for the moving stage, which reduces the natural frequency, and hence the maximum attainable speed of the stage. Another attempt was made to decouple the x and y motions in [17] using a decoupling mechanism. However, these motions were still coupled with the θ motion, and the use of the decoupling mechanism resulted in limited rotational motion. Therefore research efforts were shifted towards resolving the cross-coupling issues by improving control strategies. Estimation and compensation of cross-coupling were utilized to improve the motion accuracy effectively.

The intrinsic cross-coupling in parallel mechanisms have been widely studied in the literature [13], [18]–[20], where it was handled as unintended motions which act as external disturbances [20]. Robust control techniques such as Sliding Mode Control (SMC) are used to reduce these disturbances. Moreover, SMC is adopted to guarantee a robust system against uncertainties and unmodeled dynamics [21], [22]. The control gain in SMC is typically set to be higher than the maximum bound of the expected disturbance to eliminate its effect. However, this approach results in high chattering phenomena, which is a major disadvantage of this type of control methods. Several studies have investigated chattering reduction through the use of disturbance observers [23]. Where in these methods, the demand on the control action is reduced and in turns alleviate the chattering. Active disturbance rejection strategy was proposed in [24] and integrated with backstepping and extended state observer to improve tracking control in nonlinear systems. The approach was applied to a robotic manipulator, and the results showed improved performance over traditional adaptive control methods. A linear disturbance observer was used in [25] along with an adaptive integral terminal third-order sliding-mode controller. The method was applied to a single-DOF mechanism to achieve high tracking performance with no chattering. Limited work has been done in the direction of disturbance observer-based control for XYθ micro/nanopositioning mechanisms due to their actuation and sensing complexity. A control approach was proposed in [26] to regulate a 3-PRR XYθ micropositioning mechanisms; however, as in [25], a linear observer was used. Another linear disturbance observer that utilized Extended State Observer (ESO) was proposed in [27] to control a VCM-based XYθ micropositioning mechanism. However, ESOs are sensitive to the sampling rate. A high sampling rate is required to maintain high control performance, which sometimes is not feasible due to hardware limitations. Since XYθ micropositioning mechanisms are highly coupled systems and inherently associated with non-linear cross-coupling, the utilization of linear observers may be unreliable.

Another issue that associated with the control of multi-DOF mechanisms is the plethora of the control parameters that need manual tuning to achieve the required performance. Manual tuning is not practical as it might risk the safety of the system by selecting unstable or highly-oscillatory parameter combinations. Moreover, the maximum attainable performance is not guaranteed. Therefore it is necessary to automate this process using an optimization algorithm.

Optimization algorithms are categorized into local and global search algorithms. Local search algorithms, especially the gradient-based ones, are having a high chance of trapping in local minima solutions, and their convergence is highly sensitive to initial values. In contrast, global search algorithms do not suffer from those disadvantages due to the derivative-free nature of those algorithms. Several global search algorithms have been proposed in the literature, such as Genetic Algorithm (GA) [28], Differential Evolution (DE) [29], Particle Swarm Optimization (PSO) [30], Spider Monkey Optimization (SMO) [31], and many others.

These algorithms try to locate the global optima of the optimization problem by deploying several search agents in the solution space. Those agents follow exploration and exploitation strategies to explore their surroundings and to find an optimal solution. These strategies are essential to avoid the local minima, which may result in a premature convergence in some algorithms. The Antlion Optimizer (ALO) proposed in [32], is one of these metaheuristic optimization algorithms that is inspired by the biological behaviour of antlions. It has a superior advantage over other algorithms as it utilizes global and local search for its exploration and exploitation phases. This combination leads to a better exploration of the search space and rapid convergence to the optimal solution. Hence, it has been adopted in this work for optimizing the control parameters. The local optima avoidance and simplicity of ALO have made it successful in solving several critical optimization problems [33]–[35].
Sliding mode control method optimization by metaheuristic methods has been investigated in several studies. A classical sliding mode control method with a boundary layer hyperbolic tangent function was proposed in [36] for tracking tasks in voltage source converter high voltage direct current (VSC-HVDC) transmission systems. Classical Modified Genetic Algorithm (MGA) and PSO were utilized to optimize the controller gains. However, the use of the tangent function will cause the tracking error to approach a maximum bound. This bound was not investigated, and the parameters that affect it were not identified. In [37], a sliding mode control was combined with a linear quadratic regulator for trajectory tracking of a helicopter system. The control gains were optimized using metaheuristic algorithms. The total variance of the control signal was used in the objective function to overcome the chattering issue. However, that increased the tracking error because of the trade-off nature of the selected objective function. Moreover, the control signal exhibited large chattering due to the direct use of the signum function. A similar issue was observed in [38], where the objective function was based on a trade-off between chattering reduction and tracking error, which resulted in high chattering in the control signal. Apart from these studies, the vast majority of the literature used try and error approach for selecting sliding mode control parameters, which introduces issues with suboptimal tracking and high chattering of the control signal.

Based on what has been discussed, it can be summarized that linear disturbance observers and manual tuning methods are not practical to reduce cross-coupling and achieve optimal performance in XYθ micropositioners. Moreover, the bound of the tracking error in sliding mode control should be identified when chattering attenuation methods are used, and this bound should be reduced to its optimal feasible value. Thus, these factors should be considered and investigated in more reliable control approaches. The contributions of this work can be summarized as:

- A disturbance observer-based sliding mode control method is proposed for tracking tasks in micropositioning systems with optimized gains to reduce error bound.
- Nonlinear disturbance observer is utilized to reduce the demand on the switching control gain to be just higher than the disturbance estimation error. Thus, that reduces the chattering effect on the system.
- The time convergence analysis of the robust control method is investigated, and the error is proved to be confined within a maximum bound ρ, which can be reduced by designing the control parameters.
- The parameters that affect this bound are identified and optimized in a metaheuristic optimization approach to maximize the tracking ability of the micropositioning system, and to overcome the chattering issues.

In this work, a sliding mode control scheme based on a nonlinear disturbance observer is proposed to handle trajectory tracking tasks in XYθ micropositioning mechanisms. This methodology can estimate and compensate the unavoidable cross-couplings and reduce chattering pneumonia, as these two represent significant disadvantages in such mechanisms. The control parameters are obtained by the antlion optimizer to achieve optimal performance and to reduce the demand for manual tuning. The time convergence and stability analyses are undertaken when this control methodology. Furthermore, The experimental and simulation results confirm the stability, robustness, and effectiveness of the proposed control method in reducing cross-coupling effects and improving the tracking performance in micropositioning systems.

II. MECHANISM MODELING AND IDENTIFICATION

The planar micropositioning mechanism used in this work is shown in Fig. 1. It provides two translation and one rotation. The mechanism consists of threefold rotational symmetry, where three driving mechanisms are connected to the central platform in parallel, as shown in Fig. 1c. Each driving mechanism is composed of three flexure based joints connected in series to produce a 3-DOF motion. The first joint provides an active prismatic motion in the horizontal direction, while the second joint offers a passive vertical prismatic motion, and finally, the third one yields a passive rotation. Voice Coil Motors (VCMs) induce movements in the links. Wire electric discharge machining was used to fabricate a monolithic mechanism, where Aluminum 7075-T6 was used for its reliability. The motions are measured through three heterodyne laser interferometers to track displacement and rotation in real time with high accuracy. Retroreflectors and external mirrors were used to reflect the laser beams to the interferometers and compensate for misalignment. The laser displacements are converted into platform displacements in real time and feed into the control approach for control action calculations. The cross-coupling between the axis of this micropositioning mechanism poses challenges for traditional control techniques. Thus an advance control method that estimates and compensates these uncertainties is necessary.

A. SYSTEM MODELING

Flexure based micropositioners are ideally modeled as a damped mass where the platform represented as a lumped mass, and each flexure acts as a spring [39]. Therefore, three damped mass systems can model the mechanism in this work where each system corresponds to a degree of freedom. The overall system dynamics can be described by

\[ M \ddot{\Upsilon} + C \dot{\Upsilon} + K \Upsilon = F \]  

(1)

where \( \Upsilon \) is the displacement vector and it is given by \( \Upsilon = [x, y, \theta]^T \). Mass, stiffness, and damping coefficients are described by the diagonal matrices \( M = \text{diag}(m_x, m_y, I_\theta) \), \( K = \text{diag}(k_x, k_y, k_\theta) \), and \( C = \text{diag}(c_x, c_y, c_\theta) \), respectively. Finally, \( F \) is the forces and moment vector and it is given by \( F = [f_x, f_y, M_\theta] \). This vector is related to the VCMs forces by

\[ F = J^{-1} [fvCM1, fvCM2, fvCM3]^T \]  

(2)
where $J^{-1}$ is the inverse kinematics matrix and it is given by [40]

$$J^{-1} = \begin{bmatrix} 1 & 0 & r \\ -1/2 & \sqrt{3}/2 & r \\ -1/2 & -\sqrt{3}/2 & r \end{bmatrix}$$ (3)

where $r$ is radius of the circumference circle of the stage. The generated force of the VCM is a combination of coil force $f_{\text{coil}}$ and electrical disturbances and noise lumped into a parameter $d$ as follows

$$f_{\text{VCM}_{j}} = f_{\text{coil}_{j}} + d_j(t), \quad j = 1 - 3$$ (4)

The overall system can be found from Eqs. (1 - 4) as follows

$$\ddot{\gamma} = -C'\dot{\gamma} - K'\gamma + M'J^{-1T}(f^T + d^T)$$ (5)

where $C' = \text{diag}(\frac{c_x}{m_x}, \frac{c_y}{m_y}, \frac{c_\theta}{I_\theta})$, $K' = \text{diag}(\frac{k_x}{m_x}, \frac{k_y}{m_y}, \frac{k_\theta}{I_\theta})$, $M' = \text{diag}(\frac{1}{m_x}, \frac{1}{m_y}, \frac{1}{I_\theta})$, $f = [f_{\text{coil1}}, f_{\text{coil2}}, f_{\text{coil3}}]$, and $d = [d_x, d_y, d_\theta]$. Inverse kinematics is typically used to decouple the system, which facilitates the control of each axis separately [41], [42].

Although this decoupling approach is not perfect, it reduces the complexity of the control methodology. The residual cross-couplings are augmented with the disturbance vector under a lumped disturbance parameter. Based on this method, the dynamics of each axis of motion can be described by

$$(m_\nu + \Delta m_\nu) \ddot{\nu} + (c_\nu + \Delta c_\nu) \dot{\nu} + (k_\nu + \Delta k_\nu) \nu = u_\nu + \delta(t)$$ (6)

where $\nu$ represents a given axis ($x$, $y$, or $\theta$); the control action is represented by $u_\nu$; the parameter uncertainties are given by $\Delta m_\nu$, $\Delta c_\nu$, and $\Delta k_\nu$, and $\delta(t)$ represent external disturbances that may include cross-couplings, sensing noise, drivers noise, etc. Rearranging the above equation as

$$\ddot{\nu} = -\frac{c_\nu}{m_\nu} \dot{\nu} - \frac{k_\nu}{m_\nu} \nu + \frac{1}{m_\nu} u_\nu + \frac{1}{m_\nu} (\delta(t) - \Delta m_\nu \ddot{\nu} - \Delta c_\nu \dot{\nu} - \Delta k_\nu \nu)$$ (7)

which can be rewritten as

$$\ddot{\nu} = -\frac{c_\nu}{m_\nu} \dot{\nu} - \frac{k_\nu}{m_\nu} \nu + \frac{1}{m_\nu} (u_\nu + d_\nu)$$ (8)
where $d_v$ is the lumped disturbance, and it is given by

$$d_v = \delta(t) - \Delta m_v \ddot{v} - \Delta c_v \dot{v} - \Delta k_v v$$  \hspace{1cm} (9)

The dynamics Eq. (8) can be represented as a state space system as follows

$$\begin{bmatrix} \dot{\upsilon}_1 \\ \dot{\upsilon}_2 \end{bmatrix} = \begin{bmatrix} 0 & -1/m_v \\ -k_v/m_v & -c_v/m_v \end{bmatrix} \begin{bmatrix} \upsilon_1 \\ \upsilon_2 \end{bmatrix} + \begin{bmatrix} 0 \\ 1/m_v \end{bmatrix} (u_v + d_v)$$ \hspace{1cm} (10)

where $\upsilon_1 = v$ and $\upsilon_2 = \dot{v}$.

### B. SYSTEM IDENTIFICATION

The system dynamics were experimentally identified using the nonlinear least-squares method. A 0.1 V amplitude sinusoidal signal with a frequency spectrum from 1-1000 Hz, and a sampling frequency of 10 kHz was used in open loop, to excite the system modes. The inverse kinematics was used to utilize the excitation of each axis separately. The system dynamics model is given by

$$\begin{bmatrix} X(s) \\ Y(s) \\ \Theta(s) \end{bmatrix} = \begin{bmatrix} G_{x1}(s) & G_{x2}(s) & G_{x3}(s) \\ G_{y1}(s) & G_{y2}(s) & G_{y3}(s) \\ G_{\theta1}(s) & G_{\theta2}(s) & G_{\theta3}(s) \end{bmatrix} \begin{bmatrix} U_1(s) \\ U_2(s) \\ U_3(s) \end{bmatrix}$$ \hspace{1cm} (11)

where $G_{x1}(s)$, $G_{x2}(s)$, and $G_{x3}(s)$ are the intended motions transfer functions, and the rest are cross-coupling transfer functions, and $U_1(s)$, $U_2(s)$, and $U_3(s)$ represent the components of Eq. (2). Second order models were selected for the transfer functions in Eq. 11, because they sufficiently represent the dynamics of the micropositioning stage as evident from the experimental and estimated frequency responses shown in Fig. 2. The numerical values of Eq. 11 are given in Appendix A. The system parameters for the intended motions were found based on $G_{x1}(s)$, $G_{x2}(s)$, and $G_{x3}(s)$, and they are presented in Table 1.

### III. CONTROL METHOD DESIGN

The decoupling through inverse kinematics utilized in the open-loop scheme enabled the modeling of this 3-DOF mechanism into three separate systems. Thus each axis can be controlled as an independent system. However, due to manufacturing errors, motor driver noise and disturbances, this decoupling approach will suffer from some residual cross-coupling in each axis which affects the motion accuracy. Hence, it is necessary to reduce its adverse effect. The control method proposed here will handle residual cross-coupling, uncertainty in parameters, and disturbances as a lumped disturbance induced in each axis, and it will try to estimate and compensate its effect. A nonlinear disturbance observer was used for estimating lumped disturbances present in each axis of motion. This observer is then augmented with the sliding mode control approach to improve motion accuracy. The state-space model in Eq. (10) is used for the control methodology development.

#### A. SLIDING MODE CONTROL DESIGN

The design of sliding mode control involves the design of the sliding surface, and the reaching control law [43]. The system dynamics will be reduced to the sliding surface dynamics in the sliding mode control method [44]. Thus the control system specification should be considered when designing this surface. Since tracking performance is essential in micro/nanopositioning, a sliding surface that contains an integral action is necessary. A PID surface was used in this work to serve this purpose. The control action is developed accordingly to bring the system trajectories towards the sliding surface using a switching control action. Once the trajectories reached the surface, they should be confined within a boundary of the sliding function and asymptotically approach the origin. The sliding surface is selected as

$$s(t) = k_d \dot{e}(t) + k_p e(t) + k_i \int_0^t e(\tau)d\tau$$ \hspace{1cm} (12)

where $k_d$, $k_p$, and $k_i$ are the PID coefficients, and $e(t)$ is the trajectory tracking error signal. Henceforth, the time parameter $(t)$ will be dropped for brevity. The error is described by

$$e = \upsilon_1 - \upsilon_{1des}$$ \hspace{1cm} (13)

where $\upsilon_{1des}$ is the desired signal. The control action $u_v$ consists of the equivalent control $u_{eq}$, and the switching control $u_{sw}$, as follows

$$u_v = u_{eq} + u_{sw}$$ \hspace{1cm} (14)

The systems trajectories are maintained within the sliding manifold by the equivalent control, while they are driven towards that manifold through the switching control [45]. The trajectories are successfully maintained within the sliding surface when the sliding condition, given by Eq. (15), is satisfied.

$$\dot{s} = 0$$ \hspace{1cm} (15)

For the sliding surface in (12), this condition is given by

$$\dot{s} = k_d \ddot{e} + k_p \dot{e} + k_i e = 0$$ \hspace{1cm} (16)

The equivalent control is designed to ensure this condition holds for all $t$. Substituting $\dot{e}$, in Eq. (16) produces

$$-k_v/k_d m_v v_1 = -c_v/k_d m_v v_2 + k_d/u_{eq}(u_{eq} + u_{sw}) + k_d/m_v d_v = 0$$ \hspace{1cm} (17)

The equivalent control, $u_{eq}$, is selected as

$$u_{eq} = k_v v_1 + c_v v_2 - \hat{d}_v m_v \upsilon_{1des} \frac{m_v}{k_d} (k_p \dot{e} + k_i e)$$ \hspace{1cm} (18)
where $\hat{d}_m(t)$ is the estimated disturbance. The system’s stability is investigated using the following Lyapunov function

$$V_1 = \frac{s^2}{2}$$

(19)

The sliding surface is given by a linear PID equation, and it needs to be stable. Thus, it is sufficient to have non-negative PID gains to achieve a strictly Hurwitz system and hence the stability. Moreover, the overall stability and trajectories reachability to the sliding surface are guaranteed through

$$\dot{V}_1 = s \dot{s} \leq 0, \quad s \neq 0$$

(20)

where Eq. (20) is called the reaching condition, and $\dot{V}_1$ is given by

$$\dot{V}_1 = s \frac{k_d}{m} (d_m - \hat{d}_m + u_{sw})$$

(21)

The switching function is designed to preserve the stability of the system, and to achieve exponential reaching law to the sliding surface, as follows

$$u_{sw} = -k_1 s - k_2 \text{sign}(s)$$

(22)

where $k_1, k_2 > 0$. Combining (22) with (21) gives

$$\dot{V}_1 = s \frac{k_d}{m} (\tilde{d}_m - k_1 s - k_2 \text{sign}(s))$$

(23)

where $\tilde{d}_m$ is the difference between the actual and estimated disturbance, and it is given by

$$\tilde{d}_m = d_m - \hat{d}_m$$

(24)

The reaching condition in Eq. (20), can be represented by

$$\dot{V}_1 \leq -k_1 s^2 - k_2 |s| + |\tilde{d}_m| |s| \leq 0$$

$$-k_1 s^2 - |s|(k_2 - |\tilde{d}_m|) \leq 0$$

(25)
This condition holds if \( k_2 \) is designed as
\[
k_2 > \vert \tilde{d}_v \vert \quad (26)
\]
It is worth noting that the stability of the system is determined by having the switching gain that is larger than the disturbance estimation error, rather than the disturbance bound itself. Thus, this reduction in gain bound will reduce the control signal chattering. The chattering phenomenon is strongly presented in the sliding mode control method due to the use of the signum function in the switching control. Chattering has an adverse effect on the safety of the actuators, and it is necessary to reduce its effect. Therefore the continuous function \( \tanh(s/\epsilon) \) is used instead of \( \text{sign}(s) \), where \( \epsilon \) is a design parameter. It worth noting that when \( \epsilon \) approaches zero, the \( \tanh \) function approaches the signum one. The system stability with the \( \tanh(s/\epsilon) \) function will be revisited in Section III-C.

### B. NONLINEAR DISTURBANCE OBSERVER DESIGN

As explained earlier, the cross-coupling, VCM noise, uncertainty in parameters, etc. have a meaningful presence in the displacement of each axis. Therefore it is necessary to have an observer for estimation and compensation of those uncertainties. Nonlinear Disturbance Observer (NDO) has been proven to outperform linear observers for many systems studied in the literature [46], [47]. Thus it was adopted in this work. The state-space model in Eq. (10) is rewritten as
\[
\dot{\upsilon} = f(\upsilon) + g_1(\upsilon)\upsilon_2 + g_2(\upsilon)\tilde{d}_v, \quad (27)
\]
where
\[
f(\upsilon) = \begin{bmatrix} \frac{-k_2}{m_\upsilon} & \upsilon_2 \\ \frac{-c_\upsilon}{m_\upsilon} & \upsilon_2 \end{bmatrix}, \quad g_1(\upsilon) = \frac{1}{m_\upsilon}, \quad g_2(\upsilon) = \begin{bmatrix} 0 \\ \frac{k_3}{m_\upsilon} \end{bmatrix} \quad (28)
\]
The NDO used for estimating \( \tilde{d}_v \) is designed as
\[
\dot{\tilde{d}}_v = z + p(\upsilon) \quad (29)
\]
\[
\dot{\tilde{z}} = -l(\upsilon)(g_2(\upsilon)z + p(\upsilon)) + f(\upsilon) + g_1(\upsilon)\upsilon_2 \quad (30)
\]
where \( \tilde{d}_v \) is the estimated disturbance, \( z \) is the observer’s internal state, and \( l(x) \) is the observer gain given by
\[
l(\upsilon) = \frac{\partial p(\upsilon)}{\partial \upsilon} \quad (31)
\]

**Proposition 1:** If it is assumed that disturbance dynamics changes slowly with time, and \( p(\upsilon) \) is selected such that:
\[
\dot{\tilde{d}}_v + \frac{\partial p(\upsilon)}{\partial \upsilon}g_2(\upsilon)\tilde{d}_v = 0 \quad (32)
\]
then the estimated disturbance \( \tilde{d}_v \) approaches \( d_v \) exponentially.

**Proof:** Selecting \( p(\upsilon) \) as:
\[
p(\upsilon) = k_3\upsilon_2 \quad (33)
\]
therefore
\[
l(\upsilon) = \frac{\partial p(\upsilon)}{\partial \upsilon} = [0 \quad k_3] \quad (34)
\]
and the observer dynamics is given by:
\[
\dot{\tilde{z}} = -\frac{k_3}{m_\upsilon} (z - k_2\upsilon_1 + (k_3 - c_\upsilon)\upsilon_2 + u_\upsilon) \quad (35)
\]
\[
\dot{\tilde{d}}_v = z + k_3\upsilon_2 \quad (36)
\]
differentiating Eq. (36) with respect to time gives:
\[
\dot{\tilde{d}}_v = \dot{z} + k_3\upsilon_2 - \frac{k_3}{m_\upsilon} (\dot{d}_v - \tilde{d}_v) = \frac{k_3}{m_\upsilon} \tilde{d}_v \quad (37)
\]
Differentiating Eq. (24) with respect to time and combining it with Eq. (37), results in:
\[
\dot{\tilde{d}}_v + \frac{k_3}{m_\upsilon} \tilde{d}_v = 0 \quad (38)
\]
which is equivalent to Eq. (32). It is worth noting that \( \tilde{d}_v = 0 \) in Eq. (38) since it was assumed that \( d_v \) varies slowly with time. The solution to differential equation given in Eq. (38) is found as
\[
\tilde{d}_v = \exp(-k_3/m_\upsilon t) \tilde{d}_v(t_0) \quad (39)
\]
which converges to zero exponentially with time if \( k_3 > 0 \).

**Proposition 2:** If the single-axis dynamics given in Eq. (10) is considered with the NDO based sliding mode control approach proposed in Eqs. (18), (22), (35), and (36), then the overall system is stable and the control approach attracts the system’s trajectories towards the sliding surface.

**Proof:** Finding a positive semi-definite Lyapunov function candidate, which involves trajectory tracking and disturbance estimation errors, is sufficient to prove this proposition. Thus, the following Lyapunov function is proposed:
\[
\dot{V}_2 = V_1 + \frac{\tilde{d}_v^2}{2} \quad (40)
\]
differentiating Eq. (40) with respect to time gives:
\[
\dot{V}_2 = \dot{V}_1 + \tilde{d}_v \dot{\tilde{d}}_v \quad (41)
\]
\[
= \dot{V}_1 - \frac{k_3}{m_\upsilon} \tilde{d}_v^2 \quad (42)
\]
\[
\leq -k_1\tilde{d}_v^2 - |s| (k_2 - |\tilde{d}_v|) - \frac{k_3}{m_\upsilon} \tilde{d}_v^2 \leq 0 \quad (43)
\]
which holds if the condition in Eq. (26) is satisfied.

The overall closed loop system block diagram is shown in Fig. 3, where the micropositioning system dynamics equation that is used in optimization and simulation is given by Eq. (11).

### C. TIME CONVERGENCE ANALYSIS

The time convergence of the sliding function is investigated in this section when the disturbance observer, and chattering reduction methods are used. It follows from Eq. (42), with the substitution of \( \tanh(s/\epsilon) \) in \( \dot{V}_1 \) for chattering reduction, the \( \dot{V}_2 \) is rewritten as:
\[
\dot{V}_2 = s \frac{k_d}{m_\upsilon} (\tilde{d}_v - k_1s - k_2 \tanh(s/\epsilon)) - \frac{k_3}{m_\upsilon} \tilde{d}_v^2 \quad (44)
\]
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FIGURE 3. The overall closed loop system.

\[
\dot{V}_2 \leq -k_1 s^2 - \frac{k_3}{m_u} \tilde{d}_u^2 + |s| |\tilde{d}_u| - k_2 s \tanh(s/\epsilon)
\]

\[
= -k_1 s^2 - \frac{k_3}{m_u} \tilde{d}_u^2 + |s| |\tilde{d}_u| - k_2 |s| + k_2 |s|
\]

\[-k_2 s \tanh(s/\epsilon) \quad (45)\]

Lemma 1 [48]: The following inequality holds for all \( s, \epsilon > 0 \),

\[
0 \leq |s| - s \tanh(s/\epsilon) \leq \delta \epsilon
\]

where \( \delta \) is a constant that satisfies \( \delta = e^{-(\delta+1)} \), hence \( \delta = 0.2785 \).

Thus, Eq. (45) is written as:

\[
\dot{V}_2 \leq -k_1 s^2 - \frac{k_3}{m_u} \tilde{d}_u^2 - |s| \left( k_2 |\tilde{d}_u| + k_2 \delta \epsilon \right) \quad (46)
\]

with the consideration of the condition in Eq. (26), it can be found that

\[
\dot{V}_2 \leq -k_1 s^2 - \frac{k_3}{m_u} \tilde{d}_u^2 + k_2 \delta \epsilon \quad (47)
\]
\[ \dot{V}_2 \leq -\eta \left( \frac{s^2}{2} + \frac{d_v^2}{2} \right) + k_2 \delta \varepsilon \]  

which is equivalent to:

\[ \dot{V}_2 \leq -\eta V_2 + k_2 \delta \varepsilon \]  

where \( \eta = 2\min(k_1, k_3/m_\nu). \) The solution of Eq. (49) according to Lemma 2 is given by:

\[ V_2(t) \leq \rho + (V_2(t_0) - \rho) e^{-\eta(t-t_0)} \]  

where \( \rho = k_2 \delta \varepsilon / \eta, \) and it represents the maximum bound of the tracking error. Thus the sliding mode function is globally uniformly ultimately bounded. Moreover, the error bound \( \rho \) can be reduced by designing \( k_1, k_2, k_3, \) and \( \varepsilon. \)

Sliding mode chattering phenomena has a severe influence on the safety of the closed-loop system if not attenuated. Attenuation methods were proposed in the literature to reduce its impact. These methods cause the error to approach a given bound rather than zero. The parameters that affect this bound was not thoroughly identified and optimized in the literature towards optimal tracking. Thus, this bound \( (\rho) \) was theoretically derived in this section, and the parameters that affect it were established. These parameters are usually tuned in a try and error approach, which does not guarantee optimal performance. In this study, they are optimized to achieve better tracking performance and thus reducing \( \rho. \) 

**Lemma 2 [49]:** Let \( V, f : [0, \infty) \to \mathbb{R}, \) if \( V \leq -\eta V + f, \) \( \forall t \geq t_0 \geq 0, \) then \( V(t) \) is bounded by the following function for any finite non-negative constant \( \eta \)

\[ V(t) \leq e^{-\eta(t-t_0)}V(t_0) + \int_{t_0}^{t} e^{-\eta(t-\tau)}f(\tau)d\tau \]  

**Proof:** Let \( \mu(t) = \dot{V}(t) + \eta V(t) - f(t), \) where \( \mu(t) < 0, \) then:

\[ \dot{V}(t) = -\eta V(t) + f(t) + \mu(t) \]  

integrating Eq. (52) with respect to time gives:

\[ V(t) = e^{-\eta(t-t_0)}V(t_0) + \int_{t_0}^{t} e^{-\eta(t-\tau)}f(\tau)d\tau \]

\[ + \int_{t_0}^{t} e^{-\eta(t-\tau)}\mu(\tau)d\tau \]  

since \( \mu(t) < 0, \) then \( \forall t \geq t_0 \geq 0, \) it holds that:

\[ V(t) \leq e^{-\eta(t-t_0)}V(t_0) + \int_{t_0}^{t} e^{-\eta(t-\tau)}f(\tau)d\tau \]

and that completes the proof.

**IV. CONTROLLER OPTIMIZATION WITH ALO ALGORITHM**

ALO mimics the foraging behavior of antlions during the larvae stage of their life cycle. Antlion excavates a funnel-shaped pit and hides at its bottom by coving itself with sand, as shown in Fig. 4. This pit forms a trap for ants that roam the area. Once an ant falls down the trap, it will find it difficult to escape due to the sharp edges of the trap. Then, antlion throughs sand on the trapped ant to prevent it from escape and to slide it down towards its jaws. Once the antlion captures its prey, it will consume it, and discard the remains. Then it will repair the pit and prepare it for the next hunting cycle.

ALO algorithm has two populations: antlions and ants, both collaborate to solve the optimization problem. The ants work as exploration agents in the solution space, while antlions disguise within the space, to capture the ants. Once an antlion captures a prey at a position, it would record that position, and hence it emerges as a fitter. The parameters of the problem represent the solution space dimensions, while ants/antlions positions refer to a particular solution within that space. The locations of ants and antlions are stored throughout the propagation of the algorithm as matrices. These matrices are used by ALO operators to converge towards the solution, and they are given by:

\[
\mathbf{M}_{ant} = \begin{bmatrix}
\text{Ant}_{n, 1} & \text{Ant}_{n, 2} & \ldots & \text{Ant}_{n, d} \\
\text{Ant}_{1, 1} & \text{Ant}_{1, 2} & \ldots & \text{Ant}_{1, d} \\
\vdots & \vdots & \ddots & \vdots \\
\text{Ant}_{n, 1} & \text{Ant}_{n, 2} & \ldots & \text{Ant}_{n, d}
\end{bmatrix}
\]

\[
\mathbf{M}_{antlion} = \begin{bmatrix}
\text{AntL}_{n, 1} & \text{AntL}_{n, 2} & \ldots & \text{AntL}_{n, d} \\
\text{AntL}_{1, 1} & \text{AntL}_{1, 2} & \ldots & \text{AntL}_{1, d} \\
\vdots & \vdots & \ddots & \vdots \\
\text{AntL}_{n, 1} & \text{AntL}_{n, 2} & \ldots & \text{AntL}_{n, d}
\end{bmatrix}
\]

where \( d \) is the number of dimensions (number of parameters), and \( n \) is the number of ants/antlions. The locations of each ant and antlion are evaluated by an objective function \( f. \) Moreover, the fitnesses are found and stored for later use by the optimization processes. The fitness matrices are given by:

\[
\mathbf{M}_{OFant} = \begin{bmatrix}
f ([\text{Ant}_{1, 1}, \text{Ant}_{1, 2}, \ldots, \text{Ant}_{1, d}]) \\
f ([\text{Ant}_{2, 1}, \text{Ant}_{2, 2}, \ldots, \text{Ant}_{2, d}]) \\
\vdots \\
f ([\text{Ant}_{n, 1}, \text{Ant}_{n, 2}, \ldots, \text{Ant}_{n, d}])
\end{bmatrix}
\]
The following section describes the operations of ALO.

A. OPERATIONS OF ALO
The following operations are involved in the ALO.

1) RANDOM WALKS
The random walk of an ant in the $i$th dimension is described by:

$$X_i^k = \begin{bmatrix} 0, \sum_{j=1}^{1} (2r_j - 1), \sum_{j=1}^{2} (2r_j - 1), \\ \vdots \\ \sum_{j=1}^{N_{iter}} (2r_j - 1) \end{bmatrix}$$

(59)

where $N_{iter}$ is the maximum number of iterations, $r$ is a random number described by:

$$r_j = \begin{cases} 1 & \text{if } \text{rand} > 0.5 \\ 0 & \text{if } \text{rand} \leq 0.5 \end{cases}$$

(60)

where rand is a uniformly distributed random number. Random walks are normalized to retain them within the search space using the following expression:

$$X_{i,\text{norm}}^k = \frac{(X_i^k - a_i^k)(d_i^k - c_i^k)}{b_i^k - a_i^k} + c_i^k$$

(61)

where $a_i^k$, and $b_i^k$, are the minimum and maximum of the random walk $X_i^k$ of the dimension $i$ at the $k$th iteration, respectively. Moreover, $c_i^k$, and $d_i^k$ are the upper and lower bounds of the $i$th dimension at the $k$th iteration.

2) ANTS TRAP IN PITS
The antsions traps affect the search space of ant, and that is modeled by

$$c_i^k = \text{Ant}_{L,j,i}^k + c_i^k$$

(62)

$$d_i^k = \text{Ant}_{L,j,i}^k + d_i^k$$

(63)

3) TRAPS BUILDING
The antsions are selected based on the roulette wheel selection method. The antsions with higher fitness will have a higher probability of being selected, and hence they participate in convergence towards the optimal solution.

4) ANTS SLIDING
When an ant is trapped in the antlion’s pit, the antlion starts to throw sand grains on the ant to push it towards the bottom of the pit. This behavior is simulated by reducing the dimensions’ boundaries adaptively as follows:

$$c_i^k = c_i^k \frac{1}{l}$$

(64)

$$d_i^k = d_i^k \frac{1}{l}$$

(65)

where $l$ is an adaptive parameter that increases with the number of iteration, and it is given by:

$$l = \frac{10^n k}{N_{iter}}$$

(66)

and it changes the accuracy of the solution with the iterations.

5) HUNTING A PREY AND AMENDING THE PIT
When the antlion hunts its prey, it will consume it. If the ant has better fitness than the antlion, the antlion will relocate itself to the position of the ant as follows

$$\text{Ant}_{L,j}^k = \text{Ant}_i^k \quad \text{if } f(\text{Ant}_i^k) > f(\text{Ant}_{L,j}^k)$$

(68)

6) ELITISM
The best antlion in any iteration is selected as the elite one and kept for the next iteration. Thus, the best solution produced so far is preserved for the next iteration. The motion of the ants are updated by antlion selected from the roulette wheel, and the elite one, as follows

$$\text{Ant}_i^k = \frac{R_A^k + R_E^k}{2}$$

(69)

where $R_A^k$ is a random walk of the $i$th ant around an antlion from the roulette wheel, similarly, the ant random walk around the elite antlion is given by $R_E^k$.

B. ALO ALGORITHM
The developed control approach requires the tuning of seven parameters in each axis ($k_p, k_i, k_d, k_1, k_2, k_3, \text{ and } \epsilon$), that means it is required to tune 21 parameters in total. Based on the operators presented in the previous section, the ALO algorithm for optimizing the developed robust controller in Section III is presented by Algorithm 1. The cost function is based on mean square error, and it is given by

$$\text{cost} = \frac{1}{n} \sum_{i=0}^{n} \left( e_1^2(i) + e_2^2(i) + e_3^2(i) \right)$$

(70)
Algorithm 1: ALO Algorithm for Optimizing Control Parameters

**Require:** cost function, parameters range, n, d, Niter

**Result:** A vector of optimized control parameters

1. Initialize the two populations randomly
2. Calculate the fitness using the objective function
3. stopCondition = False
4. while not stopCondition do
5. for each ant do
6. Use Roulette wheel to select an antlion
7. Update the boundaries c and d using Eqs. (62), (63), (64), and (65)
8. Create a normalized random walk using Eqs. (59), and (61)
9. Update the ant’s position using Eq. (69)
10. end for
11. Calculate the fitness of all ants using Eq. (70)
12. Replace antlions with ants if they offer better fitness
13. Update the elite antlion
14. if (reached maximum iterations) or (reached a target fitness) then
15. StopCondition = True
16. end if
17. end while
18. Return the Elite antlion

where \( n \) is the number of simulation samples; \( e_x, e_y, \) and \( e_{\theta} \) are the trajectory tracking error in \( x \)-, \( y \)-, and \( \theta \)-axis, respectively. The number of ants are set to 25, and the number of iteration is selected as 100. The optimized parameters are given in Table 2. The cost function of the final iteration is 7.726e-13. The convergence curve of the optimization algorithm is shown in Fig. 5.

V. EXPERIMENTAL RESULTS

The experimental setup of the system is shown in Fig. 6. It consists of three subsystems: optical system, electrical system, and mechanical system.

The optical system is based on Zygo laser-based displacement measurement system. It involves a laser head and three optical measurement paths. Each path measures a linear displacement for a point on the target stage using a laser interferometer. These three points are converted into two linear and one angular displacements. Three laser interferometers were used; two on the \( x \)-axis and one on the \( y \)-axis. The two \( x \)-axis interferometers are used to detect \( x \) and \( \theta \) displacements, and the one on the \( y \)-axis is to detect \( y \) displacement only. Retroreflectors and external plane mirrors were used to reduce sensitivity to laser misalignment. The retroreflectors attached to the moving stage will reflect the incident beams in a parallel manner to off-stage plane mirrors, which in turn reflect them to the source. Then the laser beams travel through the optical components back to the interferometers to get finally picked up and transferred through the fibre optic cables to the measurement cards. Fold mirrors and beam splitters were used to facilitate laser beam steering from the laser head to the interferometers. The linear displacement measurements from the laser interferometers are converted in the software into two linear displacements (\( x \) and \( y \)), and one angular displacement (\( \theta \)).

The electrical system consists of Advantech PCI-1723 analog output data acquisition card, three VCMs VCAR0087-0062-00A, three LCAM 5/15 linear VCM drivers, and one unregulated DC power supply. The control action is supplied from the realtime software through the PCI-1723 as current commands to the VCM drivers. Each VCM driver has an internal closed-loop system to regulate the current in the VCM coil to the desired current command. The drivers require an unregulated power supply to function properly.

The mechanical system entails the 3-DOF micropositioner, VCM bases, mechanism base, and three studs to level the mechanism with the optical paths. The micropositioner was fabricated from Aluminum 7075-T6 and machined by wire electrical discharge machining technology for its high manufacturing precision.

The three systems were integrated into one feedback control system. An industrial PC deployed with Simulink realtime operating system was used to read the laser measurement and to send the VCM commands. Moreover, it also runs the control method, monitors, and records the signals. The sampling rate for the control experiment was selected as 5000 Hz, while for the system identification experiment, it was 10 kHz.

Several experiments were conducted to study the cross-coupling effect, and also to investigate the control approach performance in terms of resolution and trajectory tracking.

| Parameter | Lower bound | Upper bound |
|-----------|-------------|-------------|
| \( \lambda_0 \) | 0.5 | 1.5 |
| \( \lambda_1 \) | 15 | 25 |
| \( \lambda_2 \) | 10 | 25 |
| \( k_1 \) | 1 | 3 |
| \( k_2 \) | 0.1 | 1 |
| \( k_3 \) | 5 | 15 |
| \( \epsilon \) | 0.1 | 1.5 |

FIGURE 5. Cost function convergence curve.

TABLE 2. Optimized controller and observer parameters.
A. Cross-Coupling Experiment

The single-sided frequency spectrum was utilized to show the impact of the cross-coupling near the resonant frequency. This spectrum can clearly show the amplitude and natural frequency of the intended motions and cross-couplings. The primary axes of motion were excited individually in open loop with the aid of inverse kinematics. A 0.1 V amplitude sinusoidal signal with a frequency spectrum from 1-350 Hz,
and a sampling frequency of 10 kHz was used as input to each axis in three open-loop experiments. The experimental time response data were recorded for each experiment. Then, the fast fourier transform is utilized to obtain the single-sided frequency spectrums with the aid of MATLAB. The severity of cross-coupling can be investigated through its magnitude near the resonant frequency of the primary axes. The single-sided frequency spectrums are shown in Figs. 7-9. It can be noticed that the cross-coupling from $\theta$-axis exhibits a high magnitude at the resonance frequency of x- and y-axis. This indicates that the cross-coupling is interfering with the intended motions near the natural frequency and its effect should be attenuated.

In terms of natural frequencies, the intended motion of $\theta$-axis appears slightly higher than the other two axes. However, the cross-coupling frequency of the $\theta$-axis contaminates the intended motion of the other axes, as discussed earlier. The resonance frequency of the x-axis and y-axis are very close, which indicates the similar dynamics response in these two axes.

B. RESOLUTION TEST

The position resolution in the closed-loop scheme was experimentally investigated. A stair-step signal with 0.1 $\mu$m was used for testing the motion in both x and y axes, and 2 $\mu$rad was used to test the resolution of $\theta$-axis. No overshoot was observed in the results due to the small step size. As shown
A. Al-Jodah et al.: Antlion Optimized Robust Control Approach for Micropositioning Trajectory Tracking Tasks

in Figs. 10-12, the control approach was able to resolve a resolution of 0.1 µm in x- and y-axis, and 2 µrad in θ-axis. It must be noted that resolution is sensitive to the noise level in the laser-based measurement system, VCM-coils, VCM-drivers, and analog channels of the data acquisition card. This represents a physical limitation to the resolution improvement.

C. TRAJECTORY TRACKING VALIDATION
A whirlpool 3-DOF trajectory was used to investigate the tracking performance when all the axes are simultaneously activated. The trajectory is described by

\[ x_{\text{ref}} = 2t \cos(3t/2) \]  
\[ y_{\text{ref}} = 2t \sin(3t/2) \]  
\[ \theta_{\text{ref}} = 2t \]

where it has a diameter of 100 µm, and a height of 50 µrad when \( t \) reaches 25 s.

It can be seen from Fig. 14 and Fig. 15 that the SMC-NDO offers better tracking performance for both x and y axes than the classical SMC. As evident from Table 3, the SMC-NDO had improved the tracking by 91%, and 92%, for x- and y-axis, respectively. The error levels are comparable in the θ-axis as shown in Fig. 16, however, SMC-NDO was less sensitive to signal amplitude. The SMC-NDO achieved 49% improvement for θ-axis when compared with SMC. The control actions of the three axes are shown in Figs. 17-19. In these figures, the SMC-NDO exhibit higher control action than its counterparts as it provides disturbance compensation. Moreover, it was faster than the one from the SMC. Furthermore, the control signal for both methods showed less chattering due to the use of the tanh function.
The disturbance in mechanical systems can be estimated by rewriting Eq. (8), as follows [50]:

\[ d_\nu(T) = m_\nu \ddot{\nu}(T) + c_\nu \dot{\nu}(T) + k_\nu \nu(T) - u_\nu(T - 1) \quad (74) \]

However, this approach heavily depends on the sampling rate and the estimation accuracy of the acceleration signal, which may not be practical for many systems. The estimated disturbance from the NDO was compared with the computed one given in Eq. (74). The acceleration signal in Eq. (74) was estimated using a digital differentiator with a low pass filter. The results are presented in Figs. 20-22. It can be noted from these results that the disturbance dynamics follow a similar shape of the reference signal. Moreover, the disturbance was changing slowly, which makes the assumption in Proposition 1 holds for all time. The disturbance estimated by the NDO was smoother than the computed one, especially in \( \theta \)-axis. That indicates the effectiveness of the NDO method.

Next, the accuracy of the simulated model was investigated in a comparative study with the experimental results. The SMC-NDO control method was utilized in the closed-loop feedback system, and the tracking error was used as a comparative index. The tracking errors of the simulated and experimental system are shown in Fig. 23. It can be noticed that the system’s actual error levels were modeled accurately by the simulated system. However, the simulated system error signals were much smoother than the experimental ones. That is mainly ascribed to the noise accompanying the experimental system signals. Thus, the simulated system’s error curves appeared almost matching the zero line, while the experimental system’s error curves exhibited small fluctuations around that line.
It can be concluded that the optimized control approach was able to provide high performance in both resolution and trajectory tracking experiments. Moreover, the cross-coupling effect is quite prominent in the tracking performance when the disturbance observer was not used. That was evident from the comparison of the SMC with the SMC-NDO. The SMC gains $k_1$ and $k_2$ were kept the same as in the SMC-NDO as increasing them resulted in oscillatory behavior of the mechanism. This can be attributed to the larger chattering that entered the system. This was avoided by the NDO as it estimates and compensates for the adverse effect of the cross-coupling disturbances without the need to have a larger controller gain. In fact, the use of the NDO reduced
the condition of having a gain that is larger than the bound of disturbance to a gain that is larger than the bound of the disturbance estimation error, which is much smaller. Thus the proposed method provides promising results for improving the tacking tasks of multi-DOF micro/nanopositioners.

VI. CONCLUSION

This paper presented the design, optimization, and analysis of a robust control technique for multi-DOF micropositioning. A nonlinear disturbance observer was merged with a sliding mode control approach to compensate the unavoidable cross-couplings presented in the system. Time convergence and stability analyses were performed to investigate the maximum tracking error and feedback stability, respectively. Manual tuning of a high number of controller parameters could result in suboptimal performance. Thus the antlion optimizer algorithm was used to automate the tuning process. Experimental results revealed that the developed control methodology provided better performance when compared with the classical sliding mode control, which is generally used for similar systems. Moreover, the experimental and simulated results were consistent, which indicates the accuracy of the modeling technique. The control method developed in this paper can be adopted to improve the tracking results for multi-DOF micro/nanopositioners that suffer from cross-coupling, parameter uncertainty, and disturbances. In future work, the proposed control method will be implemented to control coarse and fine motions in multi-DOF micropositioning stages.

APPENDIX A

Dynamic system transfer functions are given below

\[
G_1(s) = \frac{27.72}{s^2 + 32.86s + 3.772e04}
\]

\[
G_2(s) = \frac{-4.933e-05s + 0.6427}{s^2 + 16.17s + 3.994e04}
\]

\[
G_3(s) = \frac{0.606}{s^2 + 47.24s + 4.778e04}
\]

\[
G_4(s) = \frac{0.0482}{s^2 + 0.0482s + 3.814e04}
\]

\[
G_5(s) = \frac{27.48}{s^2 + 32.29s + 3.693e04}
\]

\[
G_6(s) = \frac{1.039}{s^2 + 40.68s + 4.42e04}
\]

\[
G_7(s) = \frac{0.1891s + 12.35}{s^2 + 22.54s + 4.11e04}
\]

\[
G_8(s) = \frac{-0.0573s - 19.17}{s^2 + 30.09s + 4.787e04}
\]

\[
G_9(s) = \frac{48.98}{s^2 + 97.96s + 5.215e04}
\]

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