Experimental Study on the Transition Characteristics and Criterion From Wall-Peak to Core-Peak Phase Distribution in Vertical Rod Bundles

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Aiming at understanding the phase distribution characteristics and developing the transition criterion from wall-peak to core-peak phase distribution in a rod bundle channel, air–water two-phase flow experiments were conducted in 5 × 5 rod bundles in the Interfacial Evolution Research Facility at Chongqing University (IERFC). Based on the experimental data, the influences of gas velocity, liquid velocity, mixing vane spacer grid (MVSG), and geometrical size on phase distribution have been analyzed in detail. With the increasing superficial gas velocity and decreasing liquid velocity, the wall-peak phase distribution turned to core-peak. The wall-peak phase distribution was enhanced by an MVSG, and the transition from the transitional phase distribution to the wall-peak phase distribution appeared when the air–water mixture flowed through the MVSG. The gap size was the key factor for the transition of phase distribution in rod bundles. Moreover, the transition criterion from wall-peak to core-peak phase distribution was developed based on present experimental data and the data in the literature, which was also verified based on the limited data. More experiments were recommended to focus on the detailed phase distribution in the rod bundle channel with different geometrical sizes.

Keywords: phase distribution, wall-peak, core-peak, two-phase flow, rod bundles

HIGHLIGHTS

- The typical wall-peak and core-peak phase distribution characteristics have been analyzed in vertical rod bundles.
- The influences of gas velocity, liquid velocity, spacer grid, and geometrical size on phase distribution have been discussed.
- The mixing vane spacer grid promoted the transitional phase distribution to convert into wall-peak due to the shear force, stronger turbulence, secondary flow, and smaller bubble size.
- The transition criterion from wall-peak to core-peak phase distribution was developed for rod bundle channels with different geometrical sizes.
INTRODUCTION

As the common phenomena in chemical industry, petrochemical industry, nuclear power, and refrigeration, gas–liquid two-phase flows attracted much attention and were intensively investigated numerically and theoretically. As a complex and open geometry, rod bundle channel was widely applied in the nuclear reactor, heat exchanger, and chemical reactor. Thus, it is crucial to make clear the flow resistance, heat transfer characteristics, chemical reaction rate, and critical heat flux in rod bundles, which is of great significance for the safety and efficiency of the equipment. Furthermore, these crucial properties are always affected by the phase distribution characteristics.

Phase Distribution Characteristics in Circular Pipe

A large amount of work focused on phase distribution in conventional channels, especially in the circular pipe. Serizawa et al. (1975a), Serizawa et al. (1975b), and Akimi et al. (1988) studied the local characteristics of air–water two-phase flow in a round pipe with the diameter of 60 mm experimentally. And two typical phase distribution patterns were identified: wall-peak and core-peak phase distributions. For wall-peak phase distribution, bubbles tended to aggregate near the wall and the near-wall-peaks of void fraction profiles appeared. However, the core-peak phase distribution showed the void fraction peaks at the channel center. Ishii et al. (Hibiki and Ishii, 1999; Hibiki et al., 2001) also found the wall-peak and core-peak phase distributions for air–water two-phase flows in 25.4 and 50.8 mm pipes. Based on the wire mesh sensor, Prasser et al. (2007) presented the evolution of the phase distribution structure in the large pipe with the inner diameter of 195 mm, which showed wall-peak and core-peak void fraction profiles for air–water and steam–water (6.5 MPa) two-phase flows.

Some studies were also devoted to making clear the transition characteristics and criteria of phase distribution. Serizawa et al. (1975a), Serizawa et al. (1975b), and Akimi et al. (1988) demonstrated that the phase distribution pattern was determined by bubble size. Moreover, Zun et al. (1988) summarized the phase distribution data in round pipes with the diameter ranging from 20 to 86.4 mm and developed the phase distribution pattern map in the superficial liquid velocity vs. superficial gas velocity diagram. In addition, Mendez-Diaz et al. (2012) developed the transition criterion from wall-peak to core-peak phase distribution in a circular pipe, which was based on the critical bubble Reynolds number \[ Re = \frac{(v_l - v_g)D_{hp}}{\mu} < 1500 \] and Weber number \[ We = \frac{(v_l - v_g)^2D_{hp}}{\sigma} < 8 \]. However, it was difficult to adopt the critical bubble Reynolds number and Weber number to predict the phase distribution patterns directly because it was difficult to acquire or calculate the bubble diameter at the working condition, which was determined by many factors, such as the flow regime and gas and liquid velocities.

Phase Distribution Characteristics in Rod Bundles

Compared with those in a round pipe, the experimental and theoretical studies on phase distribution in the complex channel were scarce, especially those in rod bundles. Hosokawa et al. (2014) measured the local void fraction with the double sensor conductivity probe in detail in 4 × 4 rod bundles, which showed the wall-peak and core-peak phase distributions. With the help of the sub-channel void sensor (SCVS), Arai et al. (2012) discovered the small bubbles tended to migrate toward the rod gap. Based on the four-sensor conductivity probe, Paranjape et al. (2010) and Yang et al. (2013) also presented the wall-peak and core-peak phase distributions in 8 × 8 rod bundles. Yun et al. (2008) reported that bubbles gathered near the rod wall in sub-cooled boiling in 3 × 3 rod bundles; and the bubble layer and void fraction peak values were influenced by heat flux and mass flow rate. Ren et al. (2018a) and Ren et al. (2019) presented the detailed wall-peak void fraction profiles for bubbly flow and core-peak phase distribution for cap bubbly flow in 5 × 5 rod bundles. According to Arai et al. (2012) and Lucas et al. (2007), small bubbles were pushed to aggregate near the rod wall by lift force (Tomiyama, 1998; Tomiyama et al., 2002), while large bubbles were kept away from walls by wall lubrication force (Antal et al., 1991). Based on the above introduction, the schematic of typical wall-peak and core-peak phase distributions in rod bundles is presented in Figure 1, in which the blue circles represent the rods.

The spacer grid was an important component of rod-type fuel assembly, which improved the flow turbulence, heat transfer efficiency, and critical heat flux for the nuclear reactor. Yang et al. (2013) pointed out that the simplified spacer grids without mixing vanes produced stronger turbulence and made the large bubbles break up. Ren et al. (2018a) demonstrated that, for the wall-peak void fraction profiles, mixing vane space grids (MVSGs) enhanced the wall-peak phenomenon by giving rise to the larger void fraction peak values near the rod wall at the downstream of the MVSG.

Lateral Forces Acting on Bubbles

Essentially, the phase distribution was determined by the lateral forces acting on bubbles, which affected the bubble migrating direction and behaviors. According to Lucas et al. (2007), Liao et al. (2015), and Rzehak and Krepper (2013), the bubble lateral force included lift force, wall lubrication force, and turbulent disperse force. The lift force was induced by the liquid velocity gradient around the bubble, whose direction was vertical to liquid velocity. The lift force coefficient \( C_L \) was positive in the co-current upward flow, and the lift force was toward the direction of decreasing liquid velocity. Tomiyama (1998) and Tomiyama et al. (2002) acquired the correlation of the lift force coefficient by analyzing the single bubble motions in the shear flow field of high-viscosity liquid and predicted that the coefficient of lift force would be negative when the bubble size was larger than 5.8 mm (Lucas et al., 2007). The bubbles were pushed back to the main flow by the wall lubrication force when near the wall. In another way, the wall lubrication force prevented bubbles from “passing through” the wall due to the effect of lift force. On the basis of the wall lubrication force correlation developed by Antal et al. (1991) and Hosokawa et al. (2002), the wall lubrication force was determined by the bubble size, bubble Reynolds number, and Eötvös number. The turbulent dispersion force was induced by the liquid turbulence and
vortexes acting on bubbles (Ishii and Zuber, 1979; Burns et al., 2004), which was associated with the bubble size, void fraction, relative velocity, bubble Reynolds number, and Eötvös number. As discussed above, the total lateral forces acting on bubbles were affected by many factors, such as the bubble size, void fraction, liquid turbulence, bubble Reynolds number, and Eötvös number.

To sum up, although some studies were conducted on the phase distribution characteristics in different rod bundles with the help of different measuring sensors by different researchers, there was no experimental study focusing on the transition mechanisms and criterion from wall-peak to core-peak phase distribution in rod bundles. Compared with that in a circular pipe, two-phase flow in rod bundles was more complex for the limited effect of sub-channel size on large bubbles, the influence of spacer grid, stronger turbulence, and secondary flow.

Therefore, it is of great significance to make clear the transition mechanisms and develop the transition criterion from wall-peak to core-peak phase distribution. In this paper, the air–water two-phase flow experiments were performed to acquire the detailed phase distribution characteristics to reveal the influencing mechanisms of different factors acting on the phase distribution. On the basis of the measured data and existing experimental data from the literature, the empirical correlation for the transition from wall-peak to core-peak phase distribution was developed.

**EXPERIMENTAL SETUP**

**Test Loop**

The gas–liquid two-phase flow experiments were performed in the Interfacial Evolution Research Facility at Chongqing University (IERFC), as shown in Figure 2. The maximum water volumetric flow rate was 30 m$^3$/h, while the maximum air mass flow rate reached 3,000 SLM (standard liters per minute). In order to produce uniform small bubbles at the inlet of the test section, the air–water mixer was designed, which consisted of four porous metal tubes. Moreover, the phase distribution characteristics at the inlet (Port 0 shown in Figure 3) could be referred from Ren et al. 2018a. More information about the experimental setup could be found in the authors’ previous research (Ren et al., 2018a; Ren et al., 2018b; Ren et al., 2018c; Ren et al., 2018d; Ren et al., 2018e; Liu et al., 2018; Ren et al., 2019; Ye et al., 2019).

**Test Section**

The test section was made of transparent PMMA (polymethyl methacrylate). The width and length of the square casing tube were 66.1 and 1,500 mm, respectively, and the rod diameter was 9.5 mm, while the rod gap size was 3.1 mm. It should be noted that the gap size played an important role in confining the bubble motion. Two kinds of spacer grids were adopted in the test section: simplified spacer grid [SSG, different from that in Yang et al. (2013)] and mixing vane spacer grid (MVSG). The structure of the SSG is shown in Figure 4, while that of the MVSG can be found in Chen et al. (2017). Detailed description of the test section could be found in Ren et al. (2018a) and Ren et al. (2019).

As shown in Figure 3A, six measuring ports (Ports 0–5) were set for a miniaturized four-sensor conductivity probe (MFSCP) at different axial locations (10.7, 50.6, 64.2, 76.8, 90.5, and 115.8 L/D). It should be noted that, to avoid the disturbance on the flow field, only one MFSCP was installed to measure the local two-phase flow parameters. The moving line of the MFSCP is shown in Figure 3B and Figure 1, and the distance between two neighboring measuring points was about 1.0 mm. The MFSCP was designed based on the large difference of conductance between gas and liquid, which consisted of a stainless steel tube and four acupuncture needles with different lengths. Moreover, the uncertainty of MFSCP was related to the uncertainty of measured voltage, bubble number, sample
frequency, and time. Based on the error propagation model, the uncertainty of measured void fraction was about 0.67%. The processing data were demonstrated to be credible with the relative errors of area-averaged void fraction and superficial gas velocity as about 18.5 and 17.8%, respectively. More detailed information on the data processing and verification of the MFSCP could be found in authors' previous researches (Ren et al., 2018a; Ren et al., 2019; Ren et al., 2021).

Test Conditions

The experiments were conducted at the stable flow condition with the preset gas and liquid mass flow rates, which were controlled by the presupposed test conditions shown in Figure 5. And the presupposed superficial gas and liquid velocities in the test conditions were determined on the purpose of covering a larger range of flow velocities and flow regimes. The flow regime transition lines for gas-liquid flow in rod bundle channel proposed by different researchers were also shown in Figure 5, which includes the global flow regime map proposed by Paranjape et al. (2008) based on a plate-type impedance void meter, the theoretical global flow regime transition criteria developed by Liu and Hibiki (2017), and the inner sub-channel flow regime map acquired by Ren et al. (2018d) based on a sub-channel impedance void meter.

RESULTS AND DISCUSSIONS

Typical Phase Distribution Characteristics in Rod Bundles

Compared with a circular pipe, the rod bundle channel had more rod walls and produced special phase distribution features. The typical wall-peak and core-peak phase distributions in rod bundles are presented in Figures 6, 7. It should be noted \( j_g \) denotes the local superficial gas velocity, while \( j_l \) is the superficial liquid velocity. As shown in Figure 1A, the wall-peak phase distribution meant that the bubbles gathered and flew near the rod walls, which resulted in the peaks of void fraction profiles located near the rod gaps as shown in Figure 6. On the contrary, as shown in Figure 1B, the core-peak phase distribution indicated that the bubbles were more likely to gather and flow in the center of the sub-channels, which gave rise to the peaks of void fraction.
profiles near the sub-channel center as shown in Figure 7. Wall-peak phase distribution was observed at the flow condition with a lower gas velocity and higher liquid velocity as shown in Figure 6, while the core-peak pattern appeared at the flow condition with a higher gas velocity and lower liquid velocity as shown in Figure 7.

The phase distribution pattern was determined by many factors (Akimi et al., 1988), such as the void fraction, flow regimes, gas velocity, liquid velocity, and bubble size. Serizawa et al. 1975a, Serizawa et al. 1975b, and Mendez-Diaz et al. 2012 reported that phase distribution was mainly affected by bubble size. And the transverse migration of bubbles was determined by the lateral forces in circular pipes (Tomiyama et al., 2002). Furthermore, the bubble lateral forces were affected by bubble size greatly, such as lift force (Tomiyama et al., 2002) and wall lubrication force (Tomiyama, 1998). Therefore, it was necessary to put emphasis on the bubble size when discussing phase distribution characteristics.

As shown in Figure 6, the void fraction peak values increased with flow development in the axial direction, while the bubble chord length did not show large change but remained at about 1.3 mm. Therefore, it was concluded that the phase distribution was determined not only by bubble size but also by other factors, which would be analyzed in The Factors Acting on Phase Distribution. As can be seen in Figure 6, there were some hollows at some peaks of the void fraction profiles at Port 5. It was inferred that some small bubbles coalesced into larger
bubbles and larger bubbles tended to move to the sub-channel center under the combined effect of lift force and wall lubrication force; then, hollows at some peaks appeared under the complex effects of the wall-peak phase distribution and the limitation of gap size.

The core-peak phase distribution profiles are shown in Figure 7. However, due to the strong turbulence and secondary flow, the peaks were not located at the sub-channel center exactly. And the bubble chord length increased from about 2 to 3.5 mm with flow development for bubble coalescence. According to Tomiyama et al. (2002), the lift force value changed from positive to negative when the bubble size was larger than 5.8 mm in air–water two-phase flows. Obviously, it could not be applicable to the present multi-bubble flow system in rod bundles directly. However, when compared to the wall-peak phase distribution in Figure 6, it could be deduced that the phase distribution would change from wall-peak to core-peak with the increasing bubble size.

The Factors Acting on Phase Distribution
As discussed above, the phase distribution was related to liquid and gas velocities, flow regimes, and bubble size in the circular pipe (Serizawa et al., 1975a; Serizawa et al., 1975b; Akimi et al., 1988). As regard to the complex geometry of the rod bundle channel, the phase distribution was affected by rod diameter, gap size, spacer grid, bubble size, gas and liquid flow rates. In this

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**FIGURE 6** | Characteristics of wall-peak phase distribution. (A) Void fraction. (B) Bubble chord length.

**FIGURE 7** | Characteristics of core-peak phase distribution. (A) Void fraction. (B) Bubble chord length.
section, the influencing factors acting on phase distribution will be analyzed, including superficial gas velocity, superficial liquid velocity, MVSG, and geometrical size.

**Superficial Gas Velocity**
As shown in Figure 8, the wall-peak phase distribution changed to core-peak with the gas velocity increasing at $j_g = 1.00$ m/s, and the critical superficial gas velocity was in the range from 0.17 to 0.67 m/s. Meanwhile, the void fraction increased from about 0.02 to 0.36, and the bubble chord length increased from about 1 to 3.6 mm. With the increasing gas velocity, void fraction and bubble number increased, which resulted in the larger collision frequency and more coalescences among bubbles. Because of the wall lubrication force and limitation of gap size, the large bubbles migrated toward the sub-channel center, which resulted in the core-peak phase distribution. To sum up, the superficial gas velocity, bubble size, and void fraction played a positive role in the transition from wall-peak to core-peak phase distribution.

**Superficial Liquid Velocity**
With the increasing superficial liquid velocity, the phase distribution characteristics at $j_{atm} = 0.20$ m/s are shown in Figure 9. It should be noted that $j_{atm}$ represented the superficial gas velocity at the atmosphere pressure. The local superficial gas velocity $j_g$ was different because of the different local pressures. The core-peak phase distribution was not so apparent at $j_g = 0.50$ m/s, $j_g = 0.19$ m/s, which belonged to cap bubbly flow according to the sub-channel flow regime map developed by Ren et al. (2018d). Because the void fraction values at the sub-channel centers were larger than those at the adjacent gaps, it was still deemed as the core-peak phase distribution. The typical wall-peak phase distribution appeared with the increasing liquid velocity as shown in Figure 9A, while the bubble chord length decreased from about 2.5 to 1.2 mm as shown in Figure 9B. The increment of liquid velocity resulted in the lower void fraction, stronger turbulence, and more vortexes, which gave rise to the bubble breakup and smaller bubble size. The small bubbles tended to migrate toward the walls under the effect of the lift force, which promoted the appearance of wall-peak distribution.

**The Mixing Vane Spacer Grid**
In the authors’ previous study (Ren et al., 2018a; Ren et al., 2019), the effects of the MVSG were summarized as stronger turbulence, stronger secondary flow, bubble breakup, bubble lateral movement, low pressure region downstream of the MVSG, and recirculating flow behind mixing vanes. The influences of MVSG on the wall-peak, transitional, and core-peak phase distributions are shown in Figures 10–12, respectively. It should be noted that Ports 3 and 4 were located upstream and downstream of the MVSG, respectively, as shown in Figure 3. As shown in Figure 10, the MVSG promoted the larger wall-peak values and smaller bubble size for wall-peak phase distribution. However, the larger void fraction peak values near the wall improved the heat transfer resistance between the heated wall and main flow, which needs more attention in the design of a spacer grid. As shown in Figure 11, the transitional phase distribution showed large hollows near the rod gaps upstream of the MVSG while presented typical wall-peak features at the downstream of the MVSG. In a similar way, the smaller bubble size was produced by the MVSG for the stronger turbulence and shear force, which promoted the transition from transitional phase distribution to wall-peak phase distribution. With regard to core-peak phase distribution shown in Figure 12, the MVSG led to smaller bubble size, but the phase distribution was still maintained as the core-peak phase distribution at the downstream of the MVSG. To sum up, the MVSG enhanced the wall-peak phase distribution and promoted the transition.
from the transitional phase distribution to the wall-peak phase distribution, but it was hard to promote the transition from the typical core-peak phase distribution to the wall-peak phase distribution.

**Geometrical Size**

As discussed above, the gap size was the main factor limiting the bubble size and affecting the phase distribution. The phase distribution patterns acquired in different rod bundles are presented in Figure 13, including present data in 5 × 5 rod bundles with the gap size of 3.1 mm, Yang’s data (Yang, 2015; Yang, 2011) in 8 × 8 rod bundles with the gap size of 6.4 mm, Hosokawa’s data (Hosokawa et al., 2014) in 4 × 4 rod bundles with the gap size of 2.5 mm, Arai’s data (Arai et al., 2012) in 10 × 10 rod bundles with the gap size of 3.0 mm, and Julia’s data (Yun et al., 2008) in 3 × 3 rod bundles with the gap size of 8.4 mm. It should be noted that Julia’s data was obtained in the sub-cooled boiling flow, while all of the others’ data were acquired in air–water two-phase flow. Moreover, Yang’s data (Yang, 2015; Yang, 2011) only consisted of the two-phase flow parameters just at the sub-channel centers and rod gaps, which increased the difficulty and uncertainty in recognizing the phase distribution patterns. And the transition lines from wall-peak to transitional and core-peak phase distribution for a circular pipe in Figure 13 were proposed by Akimi et al. (1988) based on the phase distribution data in
different circular pipes. As shown in Figure 13, the transition lines in the circular pipe proposed by Akimi et al. (1988) were not fit for the gas–liquid flow in the rod bundle channel.

As shown in Figure 13B, the wall-peak phase distribution was hard to appear at low liquid velocity (not larger than 0.23 m/s), which resulted from that the liquid turbulence was not strong enough to produce small bubbles. As for Julia’s data (Yun et al., 2008), there were no core-peak flow conditions, which were attributed to the small bubble size in the sub-cooled boiling flow and large gap size (8.4 mm). Based on the comparison among present data, Yang’s data (Yang, 2011; Yang, 2015), and Hosokawa’s data (Hosokawa et al., 2014) shown in Figure 13, the transition from wall-peak to core-peak phase distribution appeared at a lower superficial gas velocity in the rod bundle channel with the smaller gap size.

The Transition Criterion From Wall-Peak to Core-Peak Phase Distribution

Based on the critical bubble Reynolds number and Eötvös number, Mendez-Diaz et al. (2012) proposed the transition criterion from wall-peak to core-peak phase distribution in a circular channel. However, it was difficult to acquire the bubble
diameter and relative velocity to calculate the bubble Reynolds number and Eötvös number in the actual two-phase flow systems, which limited their application range. Meanwhile, the effect of channel size was not considered in Mendez-Diaz’s correlation, which meant it could not be adopted in the complex rod bundle channel. Therefore, it was necessary to develop the transition criterion from wall-peak to core-peak phase distribution in rod bundles, based on which the phase distribution patterns could be identified for the specific working condition. As shown in Figure 13, Julia’s data (Yun et al., 2008) only included the wall-peak data, while the core-peak data point was far from the wall-peak data point in Arai’s data (Arai et al., 2012). Thus, only present data, Yang’s data (Yang, 2011; Yang, 2015), and Hosokawa’s data (Hosokawa et al., 2014) were adopted to

Figure 13: Influence of geometrical size on phase distribution. (A) Present data, \( p/d = 12.6/9.5 \). (B) Yang’s data (Yang, 2011; Yang, 2015). (C) Others’ data.
Based on the above discussions, phase distribution was related to many parameters, including bubble size, void fraction, gas and liquid densities, relative velocity, surface tension, distance from the bubble to the wall, liquid turbulence, bubble Reynolds number, and Eötvös number. Aiming at identifying the phase distribution based on the macro and easily acquired two-phase flow parameters, such as superficial gas and liquid velocities, geometrical size, void fraction, and gas and liquid physical properties, the factors acting on the transition from wall-peak to core-peak were divided into two groups: the enhancing factors and the restraint factors. The enhancing factors were summarized as the dimensionless number $N_g$ (expressed as Eq. 1), while the restraint factors were considered together as the dimensionless number $N_l$ (expressed as Eq. 2). As shown in Figure 14, with increasing $N_g$, the wall-peak phase distribution turned to core-peak; with increasing $N_l$, the core-peak phase distribution turned to wall-peak. Taking $N_g^{0.5}$ and $N_l$ as X and Y coordinates, respectively, the boundaries between wall-peak and core-peak phase distributions are plotted as magenta lines for present data, Yang’s data (Yang, 2015; Yang, 2011), and Hosokawa’s data (Hosokawa et al., 2014) as shown in Figure 14. The transition line correlations for different geometrical sizes were summarized as Eq. 3, which complied with Eq. 4. It was deduced that the coefficient $C$ in Eq. 4 was related to the channel size, especially the gap size. And the phase distribution was determined by the bubble size and bubble shape. Thus, the non-dimensional gap

![Figure 14](https://example.com/figure14.png)
size was developed as Eq. 5, in which the maximum spherical bubble size (Kim et al., 2000) was adopted as the standard value.

\[
N_l = a Re g We g \sqrt{\frac{g (\rho_s - \rho_g)}{p - d}},
\]

(1)

\[
N_l = Re_l We_l.
\]

(2)

\[
N_l = 3.29 \times 10^6 N_g^{0.5}, \quad p/d = 12.6/9.5,
\]

(3)

\[
N_l = 1.56 \times 10^6 N_g^{0.5}, \quad p/d = 16.7/10.3,
\]

(4)

\[
N_l = 17.28 \times 10^6 N_g^{0.5}, \quad p/d = 12.5/10,
\]

(5)

\[
N_l = C N_g^{0.5},
\]

(6)

\[
L_{g pop} = \frac{p - d}{D_g},
\]

(7)

\[
D_g = 4 \sqrt{\frac{2 \sigma}{g \rho g N_l^{1/3}}},
\]

\[
N_{pg} = \frac{\mu_f}{(p g \sqrt{L_{g pop}})^{2.2}}.
\]

Aimed at developing the dimensionless transition criterion, the data points are plotted in Figure 15 by taking the coefficient C and dimensionless gap size \( L_{g pop} \) as the coordinates. Because the phase distribution data in different rod bundle channels were scarce in the published literature, there are only three data points in Figure 15. As can be seen, with the increasing non-dimensional gap size \( L_{g pop} \), the coefficient C decreased rapidly when the gap size ranged from 2 to 3.1 mm and then decreased slowly when the gap size was larger than 3.1 mm. Although there were only three data points, the correlation between the coefficient C and the non-dimensional gap size \( L_{g pop} \) is still developed as

\[
C = 1.44 + \frac{11.92}{L_{g pop}^{0.36}} + 11112.08 e^{-18.44 L_{g pop} + 16.82}.
\]

(8)

In order to verify the transition criterion, the data acquired by Yun et al. (2008) and Arai et al. (2012) were adopted. And \( N_l/C N_g^{0.5} \) was adopted as the Y coordinate, whose value was larger than 1 for wall-peak phase distribution and smaller than 1 for core-peak phase distribution. As shown in Figure 16, the developed correlation was applicable to the data in rod bundle channel with \( p/d \) at 13/10 (Arai et al., 2012) and 16.8/10.2 (Yun et al., 2008), which demonstrated the reliability of the present transition model to some extent. It should be noted that the correlation for the transition from wall-peak to core-peak phase distribution needed more experimental data to amend and verify. More experiments were suggested to focus on the phase distribution patterns in rod bundle channels with different geometrical sizes.

**CONCLUSION**

In this work, air–water two-phase flow experiments were performed to make clear the phase distribution characteristics and develop the transition criterion from wall-peak to core-peak phase distribution in rod bundles. Based on the analysis on experimental data, the phase distributions in rod bundles were related to many factors, such as the bubble size, void fraction, gas and liquid densities, gas and liquid velocities, surface tension, distance from the bubble to the wall, MVSG, geometrical size, liquid turbulence, and bubble lateral forces. By dividing the influencing factors into the enhancing and restraint factors, the dimensionless correlation for the transition from wall-peak to core-peak phase distribution in rod bundles was developed. Some important conclusions are listed as follows:

- With the increasing superficial gas velocity and decreasing liquid velocity, the wall-peak phase distribution turned to the core-peak pattern.
- For present flow conditions, the MVSG enhanced the wall-peak phase distribution and promoted the transitional phase...
distribution to turn to wall-peak, but it was hard to promote the transition from the typical core-peak phase distribution to the wall-peak phase distribution.  

- The wall-peak phase distribution was hard to appear at low liquid velocity (not larger than 0.23 m/s) for the weak liquid turbulence according to the experimental data in the literature (Yang, 2011; Yang, 2015).

- The geometrical size of the rod bundle channel had great influence on the transition from wall-peak to core-peak phase distribution in rod bundles, especially the gap size.

- The dimensionless transition criterion from wall-peak to core-peak phase distribution was proposed based on present data, Yang's data (Yang, 2011; Yang, 2015), and Hosokawa's data (Hosokawa et al., 2014) while verified against Julia’s data (Yun et al., 2008) and Arai’s data (Arai et al., 2012).

It should be noted that the developed transition model needed much more experimental data to amend and verify. More experiments were suggested to focus on the transition from wall-peak to core-peak phase distribution in rod bundle channels with different geometrical sizes.

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**DATA AVAILABILITY STATEMENT**

The original contributions presented in the study are included in the article/Supplementary Material, and further inquiries can be directed to the corresponding authors.

**AUTHOR CONTRIBUTIONS**

Q-YR: carrying out experiments, data processing and writing draft paper. ZP: paper reviewing. PC: project administration and funding support. L-MP: paper reviewing and supervision. FZ: data processing and writing editing. MZ: project administration and investigation. HW: investigation and carrying out experiments. LW: data processing and paper revising. HH: carrying out experiments and data processing.

**FUNDING**

The authors are grateful for the support of the Natural Science Foundation of China (Grant Nos. 51660202 and 51760206) and National Key R&D Program of China (Grant No. 2018YFE0116100).
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**Conflict of Interest:** The authors declare that the research was conducted in the absence of any commercial or financial relationships that could be construed as a potential conflict of interest.

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