A systematic study on the synergistic effects of MWCNTs and core–shell particles on the physomechanical properties of epoxy resin

Ali Gharieh1* & Mir Saeed Seyed Dorraj2

Here, core–shell impact modifier particles (CSIMPs) and multiwalled carbon nanotubes (MWCNs) were used as reinforcing agents for improving the toughness and tensile properties of epoxy resin. For this purpose, emulsion polymerization technique was exploited to fabricate poly(butyl acrylate-allyl methacrylate) core-poly(methyl methacrylate-glycidyl methacrylate) shell impact modifier particles with an average particle size of 407 nm. It was revealed that using a combination of the prepared CSIMPs and MWCNTs could significantly enhance the toughness and tensile properties of the epoxy resin. Also, it was observed that the dominant factors for improving the fracture toughness of the ternary composites are crack deflection/arresting as well as enlarged plastic deformation around the growing crack tip induced by the combination of rigid and soft particles. The Response Surface Methodology (RSM) with central composite design (CCD) was utilized to study the effects of the amounts of CSIMPs and MWCNTs on the physomechanical properties of the epoxy resin. The proposed quadratic models were in accordance with the experimental results with correlation coefficient more than 98%. The optimum condition for maximum toughness, elastic modulus, and tensile strength was 3 wt% MWCNT and 1.03 wt% CSIMPs. The sample fabricated in the optimal condition indicated toughness, elastic modulus, and tensile strength equal to 2.2 MPa m1/2, 3014.5 MPa, and 40.6 MPa, respectively.

Epoxy resins, due to their great physomechanical attributes such as good chemical resistance, outstanding adhesion, and exceptional dimensional stability, are of paramount importance in various structural applications1. However, due to their high density of three-dimensional molecular structure, hardly can they resist toward growth of crack. This serious drawback limits their applications in many critical fields where a notable fracture strength or low-temperature toughness is required, such as aerospace and automotive industries2,3. To deplete the severity of this issue, a plethora of different ingredients such as liquid rubbers, core–shell impact modifier particles (CSIMPs), and rigid organic and inorganic ingredients were used as impact modifiers particles (IMPs) of epoxy resin4–7.

Generally speaking, soft IMPs (i.e. liquid rubbers and CSIMPs) could endanger significant improvement in the toughness of epoxy resin through various mechanisms such as deboning, cavitation, and crazing6,8. Nonetheless, incorporation of such IMPs in epoxy formulation could result in deterioration of other desired properties of the host polymer (such as modulus, stiffness, and tensile strength)9. On the other hand, rigid IMPs not only could enhance the toughness of epoxy resin by crack pinning, crack deflection, and deflection/bifurcation effect of growing crack, but also could boost stiffness and modulus of the host polymer10. However, to reach a satisfying level of toughness, it is inevitable to use a relatively high dosage of such IMPs in the epoxy formulation. This obligation causes a dramatic increase in viscosity and subsequently inroads serious difficulties in the processability of the obtained composite11.

Regarding the mentioned limitations of IMPs and their inherent differences from the viewpoint of toughening mechanisms, in the last decade, hybridization of different rigid and soft IMPs embedded into epoxy polymer

1Department of Polymer Chemistry, Faculty of Chemistry, University of Isfahan, Isfahan 81746-73441, Iran. 2Applied Chemistry Research Laboratory, Department of Chemistry, Faculty of Science, University of Zanjan, Zanjan, Iran. *email: a.gharieh@sci.ui.ac.ir
matrix provided outstanding opportunities to the researchers for developing high-performance nanocomposites with enhanced toughness and physicomechanical properties\textsuperscript{11–16}. The obtained ternary nanocomposite could overcome the mentioned drawbacks and cause synergistic influences on the toughness and other physicomechanical properties of the obtained composite products.

It is no doubt that outstanding attributes of carbon nanotubes such as their high tensile strength and stiffness, could remarkably enhance fracture toughness and physicomechanical properties of polymers\textsuperscript{17}. Thus, among different rigid particles, it has been demonstrated that using carbon nanotubes as rigid fillers along with other soft IMPs could culminate a notable enhancement in fracture toughness of the obtained composites. Rio et al. showed that the addition of a mixture of rigid carbon nanotube and soft polystyrene-polybutadiene-poly (methyl methacrylate) triblock copolymers led to the dramatic increase in both fracture toughness and fracture energy of the epoxy resin\textsuperscript{18}. In another attempt, it was revealed that using block copolymer could ameliorate the dispersion state of carbon nanotubes and causes a synergistic effect on the toughness of epoxy resin\textsuperscript{19}. Jojibabu et al. showed that ternary composite of triblock copolymer, modified carbon nanotubes, and epoxy resin possess a remarkable improved toughness in comparison with binary composites\textsuperscript{20}.

The technique of experimental design, due to its valuable assistance for comprehensive understanding of the process and interactive relationships between different variables, is known as a distinguished method in the engineering fields\textsuperscript{21}. Among different methods, the response surface method, which is a collection of mathematical and statistical techniques, has been used extensively to study and optimize the effect of diverse determining factors on the various parameters\textsuperscript{22}. To the best of current authors’ knowledge, there is no single published numerical and systematic study about the synergistic effects of MWCNTs and CSIMPs on the toughness and tensile properties of epoxy resin. Thus, a systematic study of the influence of multiwalled carbon nanotubes (MWCNTs) and CSIMPs on the mentioned attributes of epoxy resin is the main objective of this work. For this purpose, response surface methodology was used to find an applicable approximation function for predicting and optimization of the toughness and tensile properties of composites with various amounts of CSIMPs and MWCNTs.

Experimental

Materials. Monomers, glycidyl methacrylate (GMA), methyl methacrylate (MMA), allyl methacrylate (ALMA) from Merck Chemical Co., and butyl acrylate (BA) from Fluka were purchased and used as received. Emulsogen APS 100 from Clariant, ter-butyl perbenzoate (TBPB) from Merck Chemical Co., sodium formalde-hyde sulfoxylate (SFS), ethylene diamine tertaacetic acid (EDTA), iron (II) sulfate heptahydrate (FeSO\(_4\) \(\cdot\) 7H\(_2\)O), and ammonium persulphate (APS) from Aldrich, were used without any further purification. MWCNTs with the purity of > 95%, length of 5–15 µm, and outer diameter of 10–20 nm was purchased from Nutrino (Tehran, Iran). The epoxy resin was standard diglycidylether of bisphenol A (DGEBA) (Epon828 from HEXION) with an epoxy equivalent molecular weight between 185 g/eq and 192 g/eq. The curing agent was cycloaliphatic polyanime hardener (Epicure F205 from HEXION) with hydroxyl equivalent weight of 102–106 g/eq. Deionized water (DIW) was used in all recipes.

Characterizations. FT-IR spectrum was recorded on FT-IR BRUKER-IFS 48 spectrophotometer (Germany) using KBr pellet. Glass transition temperature (\(T_g\)) of the core and shell portions of the prepared CSIMPs were determined according to ASTM D 3418-08, by differential scanning calorimeter, DSC-Netzsch (England). The prepared dried sample was scanned in the temperature range between ~ 100 and 140 °C at a heating rate of 10 °C/min under nitrogen atmosphere. The \(T_g\) was defined as the midpoint of deflection of the baseline from the DSC thermogram. Size and external morphology of the prepared latex particles were investigated by scanning electron microscopy (SEM) with MIRA3 instrument from Tescan (The Czech Republic). Also, SEM images of the fracture surfaces of the epoxy specimens were used to assess the toughening mechanisms. The internal morphology of the prepared latex particles was studied by transmission electron microscopy (TEM) with CEM 902A ZEISS with an accelerating voltage of 80 kV (Oberkochen, Germany). Tensile properties of the dog-bone-shaped specimens were obtained by a universal testing machine according to ASTM D-638. For each sample, the data reported are the average of five measurements. Fracture energy (\(G_{IC}\)) and fracture toughness (\(K_{IC}\)) were determined using a single-edge notch bend (SENB) specimen with dimensions of 6 × 12 × 52.8 mm. The tests were performed at a rate of 10 mm/min.

Synthesis of the impact modifier particles. Soft impact modifier particles with core–shell morphology were prepared through emulsion polymerization technique in two stages. At the first step, elastomeric cores of poly (BA-ALMA) were prepared through surfactive emulsion polymerization. For this purpose, 160 g DIW, 1 g Emulsogen APS 100, 30 g BA, and 0.16 g ALMA were premixed and charged into a 250 mL, four-necked round bottom glass reactor equipped with reflux condenser, thermocouple, crescent Teflon-steel mechanical stirrer, and feeding inlets. The content of the reactor was deoxygenated by purging with nitrogen for 15 min. The temperature was raised to 80 °C and the polymerization reaction was started by the addition of solution of the initiator (0.04 g APS dissolved at 10 mL water). The conversion of the polymerization reaction was followed by gravimetric analysis of samples withdrawn from the reactor at regular time intervals. After 120 min, the final conversion of the polymerization reaction was above 99%.

In the second stage, copolymerization of MMA and GMA was carried out on the surface of the prepared elastomeric cores. For that, 200 g of the prepared latex, 9 g MMA, 1 g GMA, and 0.1 g TBPB charged into the reactor. The content of the reactor was mixed for 30 min at room temperature. Then, 10 mL of the aqueous solution of 0.02 g EDTA, 0.01 g FeSO\(_4\) \(\cdot\) 7H\(_2\)O, and 0.1 g SFS were added into the reactor. The redox emulsion copolymerization was proceeded for 3 h at 30 °C to reach conversion of > 98%. Then, the prepared latex was filtered through a 53 mm sieve and the filtrate was freezing for 12 h and freeze-drying for another 12 h.
Experimental design and fabrication of toughened specimens. The CCD of RSM was used to assess the effects of the contents of MWCNTs and CSIMPs as independent factors on the fracture toughness and tensile properties of epoxy composites. Table 1 shows the ranges and levels of these factors. Total number of 13 experiments was designed by CCD algorithm which consists of 4 cube points, 4 axial points and 5 replications of the central points in cube to check the reproducibility variance.

Table 1. Real and coded levels of variables.

| Independent factor | Symbol | Coded level |
|--------------------|--------|-------------|
| MWCNT (wt%)        | X₁     | −1.5 −1 0 1 1.5 |
| CSIMP (wt%)        | X₂     | 0 0.5 1.5 2.5 3 |

Table 2. Experimental design matrix and responses.

| Run | Factors | Response: Young’s modulus, E (MPa) | Response: tensile strength, S (MPa) | Response: fracture toughness, KIC (MPa·m^{1/2}) |
|-----|---------|----------------------------------|----------------------------------|-----------------------------------------------|
| 1   | 0.5 0.5 | 1480.680 1556.91                 | 26.02 26.17                      | 0.89 0.78                                     |
| 2   | 1.5 1.5 | 1934.51 1882.85                 | 34.45 34.36                      | 2.27 2.18                                     |
| 3   | 1.5 1.5 | 1863.62 1882.85                 | 34.96 34.36                      | 2.07 2.18                                     |
| 4   | 0.5 2.5 | 1523.7 1612.02                 | 31.46 31.32                      | 2.24 2.35                                     |
| 5   | 1.5 1.5 | 1892.91 1882.85                 | 33.39 34.36                      | 2.13 2.18                                     |
| 6   | 2.5 0.5 | 2917.6 2958.44                 | 40.35 40.73                      | 1.83 1.78                                     |
| 7   | 3 1.5 | 2745.4 2711.6                 | 38.13 37.86                      | 2.61 2.55                                     |
| 8   | 1.5 0 | 2438.14 2388.79                 | 34.02 33.73                      | 0.98 1.11                                     |
| 9   | 1.5 3 | 1762.94 1697.49                 | 30.8 30.88                       | 3.61 3.44                                     |
| 10  | 2.5 2.5 | 1928.68 1981.59                 | 31.7 31.8                        | 3.16 3.32                                     |
| 11  | 1.5 1.5 | 1927.73 1882.86                 | 34.08 34.36                      | 2.29 2.18                                     |
| 12  | 0 1.5 | 1464.27 1383.27                 | 26.55 26.6                       | 1.07 1.08                                     |
| 13  | 1.5 1.5 | 1824.21 1882.85                 | 34.99 34.36                      | 2.17 2.18                                     |

Experimental design and fabrication of toughened specimens. The CCD of RSM was used to assess the effects of the contents of MWCNTs and CSIMPs as independent factors on the fracture toughness and tensile properties of epoxy composites. Table 1 shows the ranges and levels of these factors. Total number of 13 experiments was designed by CCD algorithm which consists of 4 cube points, 4 axial points and 5 replications of the central points in cube to check the reproducibility variance.

Table 2 illustrates the details of the designed experimental conditions proposed by CCD. To find the best fitted model, the step-wise model fitting by Minitab 14 software was used. Equation 1, which is a second-order empirical quadratic polynomial model, shows the behavior of the system

\[ Y = b_0 + \sum_{i=1}^{k} b_i X_i + \sum_{i=1}^{k} b_i^2 X_i^2 + \sum_{i=1}^{k} \sum_{j=1}^{k} b_{ij} X_i X_j, \]

where \( Y \) is the predicted physicomechanical response, \( b_0 \) is the constant, \( b_i \) is the linear effect of the factor \( x_i \) (i = 1, 2 and 3), \( b_{ii} \) is the quadratic effect of the factor \( x_i \) and \( b_{ij} \) is the linear interaction effect between the input factors, \( x_i \) and \( x_j \).

To evaluate the effect of CSIMPs and MWCNTs on the physicomechanical properties of epoxy resin, specimens with different contents of these reinforcing fillers were fabricated according to the Table 2. For this purpose, definite amounts of MWCNTs and CSIMPs were added to 100 g of epoxy resin and stirred to form a uniform mixture. Then, to ensure that the fillers were uniformly distributed in the epoxy matrix, the mixture was processed by a three-roll milling (EXAKT 80E, Exakt Technologies, Germany) for 20 min via a three-roll grinder. The three-roll milling was used in gap mode with a 5 mm distance configuration between the center and apron roller. The speed of the apron roller was 260 rpm and the roller speed ratio was 6:2:1. Then, 58 g Epicure F205 as a curing agent was added to the mixture and stirred with a glass rod. Finally, the prepared mixtures were degassed by a centrifugal deaerator for 10 min at 3000 rpm. The mixtures were poured into silicon molds and a two-step curing procedure was carried out; 2 h at 40 °C then 4 h at 120 °C using a ramp rate of 10 °C/min.

Results and discussion

Preparation of impact modifier particles with core–shell morphology. The capability of emulsion polymerization in preparing colloidal particles with disparate morphologies, physical, and chemical attributes makes it a unique and enticing polymerization method\(^2\). Here, thanks to these features, impact modifier particles with elastomeric core and epoxy-functionalized plastic shell were prepared successfully. A schematic illustration of the preparation steps of the CSIMPs is shown in Fig. 1.
It is well known that using monomers such as ALMA, which has unsaturated bonds with different reactivity, could significantly enhance grafting efficiency, gel content, and structural stability of CSIMPs. Linked to these rationales, in this work, ALMA was chosen as a graftlinking monomer in the formulation of the prepared elastomeric cores of CSIMPs. To fabricate the plastic shell, redox emulsion copolymerization of MMA and GMA was occurred at the interfacial region of elastomeric cores and aqueous medium. It was suggested that using a swelling time for dissolving monomers in poly (BA-ALMA) colloidal particles, as well as proceeding the radical formation reactions at the interfacial region, could effectively minimize the probability of micellar and homogeneous nucleation. Also, it is surmised that such swelling time could significantly enhance the grafting reaction between the elastomeric core and the glassy shell. This reaction could enhance the stability of the formed shell toward dissolution and separation from the elastomeric core during mixing of CSIMPs with epoxy polymer.

The electron microscopy results of the prepared CSIMPs (Fig. 2) manifest that the employed synthesis method could successfully fabricate CSIMPs with an average particle size of 337 nm. Also, TEM images revealed that the average sizes of the core and shell are 246 nm and 45 nm, respectively. There are a plethora of reports about significant influences of the diameter of the elastomeric core and the thickness of the glassy shell on the performance of CSIMPs. For example, it has been demonstrated that by decreasing the particle size of various elastomeric impact modifiers such as carboxyl-terminated butadiene acrylonitrile (CTBN) or CSIMPs their resistance towards cavitation increased. Kim et al. showed that due to the difficulty in cavitation of rubbery core, toughening effectiveness of poly (butyl acrylate) core- poly (methyl methacrylate) shell particles decreased for particle sizes smaller than 0.2 µm. However, fracture toughness was constant in the bigger particle sizes ranges. Here, the measured average particle size of the prepared poly (ALMA-BA) core is in good accord with the size of the elastomeric core of the other prepared CSIMPs which could remarkably enhance the fracture toughness of epoxy polymer. Thus, it is surmised that the fabricated elastomeric particles could efficiently ameliorate the toughness of epoxy resin through toughening mechanisms such as induced plastic deformation and cavitation.

The most prominent role of the glassy shell of CSIMPs is making a compatible layer between the elastomeric core and epoxy matrix. This layer provides a stress bridge for transferring of the energy of the imposed load from the matrix to the rubbery core of CSIMPs. Thus, the lower thickness of the shell could remarkably facilitate the transferring stress from polymer matrix toward the rubbery core and enhance the performance of the CSIMPs. On the other hand, the adequate thickness of the formed glassy shell could guarantee the compatibility between CSIMPs and epoxy matrix and enhance the dispersion state of the CSIMPs by preventing their coalescence during the drying and compounding process. The low measured average thickness of the shell and the free-flowing state of the synthesized CSIMPs at their powdery form substantiated that the thickness of the shell is in a suitable range for meeting the cited challenges.

Figure 3a represents the FTIR spectra of the prepared CSIMPs. The adsorption peaks at 1730 cm⁻¹ and 1160 cm⁻¹ are attributed to the C=O and C–O stretching vibrations of ester groups, respectively. The absorption peaks at 1230–1280 cm⁻¹, 815–950 cm⁻¹, and 750–770 cm⁻¹, correspond to the symmetric stretching vibration and bending mode of the epoxy groups and confirm that the exploited GMA monomer could successfully functionalize the CSIMPs by epoxy rings.

DSC thermogram of the prepared CSIMPs revealed two main transition temperatures (Fig. 3b). The first transition (≈ −41 °C) was related to the T_g of the elastomeric core. The observed difference between the measured T_g of the elastomeric core and reported values for poly (butyl acrylate) could be due to its crosslinked structure and induced restriction by the grafting glassy shell of CSIMPs. The second glass transition temperature (≈ 109 °C) corresponds to the grafted poly (MMA-GMA) shell. The observed distinct differences between measured T_g's of the core and shell portions of CSIMPs confirmed that exploited monomers in each step of the preparation procedure could form discrete phases.
Modeling and optimization using response surface methodology. The results in Table 2 were used to fit the polynomial models representing the Young’s modulus (E), tensile strength (S) and fracture toughness (KIC) of the toughened specimens (responses) as a function of the contents of MWCNTs (wt%; \( X_1 \)) and CSIMPs (wt%; \( X_2 \)). The following equations express the overall predictive model in terms of the coded variables:

- \( Y_{\text{Young's modulus}} = 1882.9 + 664.2X_1 - 345.7X_2 + 164.6X_1^2 + 160.3X_2^2 - 580.5X_1X_2 \), \( R^2_{\text{total}} = 0.98 \) (2)
- \( Y_{\text{Tensile strength}} = 34.364 + 5.633X_1 - 1.423X_2 - 2.132X_1^2 - 2.059X_2^2 - 7.935X_1X_2 \), \( R^2_{\text{total}} = 0.98 \) (3)
- \( Y_{\text{Fracture toughness}} = 2.182 + 0.73826X_1 + 1.16762X_2 - 0.36754X_1^2 + 0.09146X_2^2 - 0.01181X_1X_2 \), \( R^2_{\text{total}} = 0.98 \) (4)

The importance and statistical significance of the quadratic models were evaluated by the analysis of variance (ANOVA), which has been presented in Table 3. The ANOVA includes some statistic factors such as lack of fit, \( R^2 \), and adjusted \( R^2 \). The ANOVA results (Table 2) indicated that the models were highly significant, as P-value for the models was 0.000. The high \( R^2 \) values of the models demonstrated that they were capable of accurately predicting the mechanical properties of the prepared epoxy samples in the studied range. The insignificance “lack of fit” with P-value of higher than 0.05 indicated that in the models, LOF is meaningless and the models have appropriate accuracy for predicting the results. All terms in the regression models are not equally important. The significance of each coefficient was determined by P values (probability), which are listed in Table 3. The
probability values less than 0.05 call for the rejection of the null hypothesis, indicating that the particular term significantly affects the mechanical properties of the coatings.

The obtained response surface and contour plots provide a procedure to predict the mechanical properties of the prepared epoxy specimens reinforced with various amounts of MWCNTs and CSIMPs. As it can be seen obviously in Fig. 4a, by increasing the content of MWCNTs, due to their intrinsic rigidity and significantly high Young's modulus, the E values of the fabricated epoxy composites increased remarkably. Also, it can be seen that the addition of CSIMPs could not effectively alter Young's modulus of the host polymer up to 2.2 wt%. The plausible explanation for this observation could be due to the relatively low dosage of the used CSIMPs and also their ability to establish covalent linkages with epoxy matrix. The latter phenomena could effectively form spatial hindrance for polymer chains and increase the crosslink density of the final composite. Nevertheless, this effect could partially be compensated by the elastomeric core of the CSIMPs and result in the observed plateau region of modulus as a function of the content of CSIMPs. However, at higher levels of CSIMPs (> 2.2 wt%), an increase in the modulus of the prepared composites was observed which could be attributed to the increasing in the content of the glassy functional shell of the CSIMPs in the composites structures. As it can be seen clearly from the obtained contour plot, the measured modulus of the fabricated ternary composites could be explained by the cited rationales for individual effects of MWCNTs and CSIMPs.

It is well known that introducing MWCNTs in the epoxy matrix could exert significant influence over the tensile strength of the obtained composite. This influence could be seen as a remarkable improvement in the tensile strength by increasing the content of MWCNTs in Fig. 4b. Also, it is seen that the addition of CSIMPs causes an improvement in the tensile strength of the host polymer. This observation could be related to two pivotal traits of CSIMPs; (i) the ability of the plastic shell for the creation of covalent bonds with epoxy matrix, (ii) crosslinked attribute of the core, which could guarantee the structural stability of CSIMPs. The obtained S values of ternary composites revealed that the effect of CSIMPs on the obtained results is more prominent than MWCNTs. In other words, at a constant concentration of MWCNTs, the addition of CSIMPs render a significant

![Figure 3. (a) FTIR spectrum and (b) DSC thermogram of the prepared CSIMP.](https://example.com/figure3.png)
decrease in the tensile strength of the obtained nanocomposite, which could be attributed to the elastomeric portion of CSIMPs. The influence of the contents of MWCNTs and CSIMPs on the fracture toughness of epoxy resin is shown in Fig. 4c. It can be seen clearly that both of the added ingredients could significantly increase the $K_{IC}$ of epoxy resin. However, as it is expected, the influence of CSIMPs is more prominent than MWCNTs. Moreover, it is observed that for the binary composites of MWCNTs/epoxy the measured fracture toughness is not directly proportional to the amounts of MWCNTs. This observation is probably due to the dominant aggregation of MWCNTs at higher concentration of this material. To put it in another way, it is well-known that due to the enormous specific surface area of MWCNTs, they have strong tendency for creating clusters within the epoxy matrix. The formed clusters of MWCNTs could decrease the interfacial surface area between the epoxy resin and rigid fillers, which consequently can reduce their interactions with growing cracks and decrease the toughening performance of MWCNTs. An enticing additional insight is the synergistic toughening effects of MWCNTs and CSIMPs. It can be seen conspicuously that the ternary composite with 3 wt% MWCNTs and 3 wt% CSIMPs possesses the highest value of fracture toughness. This observation shows that the employed rigid and soft fillers could exert significant positive influence over the fracture toughness of epoxy resin. It is substantiated that the dispersion state of MWCNTs could be improved significantly by the addition of polymeric impact modifiers. Here, it is suggested that the added CSIMPs could decrease the aggregated structures of MWCNTs and facilitate their dispersion in the epoxy matrix.

Optimization of effectual factors was mainly done to define the optimum formulation that caused the achievement of maximum $E$, $S$, and $K_{IC}$. The optimum values of selected factors were obtained by solving the regression equations (Eqs. 2–4). The optimum formulation for achieving the cited aims was found to be as follows: MWCNTs (wt%) = 3 and CSIMPs (wt%) = 1.03. The maximum mechanical properties predicted by using the optimum values of factors were $E = 3014$ MPa; $S = 40.57$ MPa, and $K_{IC}$ = $2.2$ MPa m$^{1/2}$. The tensile properties and toughness of the ternary composite in optimum condition obtained through the experiment were $E = 2970$ MPa; $S = 41.2$ MPa, and $K_{IC}$ = $2.1$ MPa m$^{1/2}$, which were in good accordance with the expected results. It can be concluded that the response surface methodology is a trustworthy tool for optimizing the mechanical properties of epoxy coatings.

Fracture surface. To assess the effect of MWCNTs and CSIMPs on the fracture toughness of the ternary composite, the fracture surface of the epoxy polymer, binary, and the optimized ternary composites were comparatively examined by SEM. As it can be seen in Fig. 5a, the neat epoxy sample exhibits a typical fracture surface for unfilled epoxy resins, i.e., smooth fracture surface with the fine line patterns which indicates generally uninterrupted crack propagation and low fracture toughness. On the other hand, for binary epoxy composite with 1.5 wt% MWCNTs (Fig. 5b), a rough fracture surface indicating a ductile fracture of the composite is observed. It has been reported that the addition of MWCNTs to epoxy matrix could significantly increase the fracture

| Term                  | Coef  | P-value |
|-----------------------|-------|---------|
| (a) Response: Young's modulus ($E$) |
| Constant              | 1882.9| 0.000   |
| wt% MWCNT             | 664.2 | 0.000   |
| wt% CSIMP             | − 345.7| 0.000   |
| wt% MWCNT × wt% MWCNT | 164.6 | 0.029   |
| wt% CSIMP × wt% CSIMP | 160.3 | 0.032   |
| wt% MWCNT × wt% CSIMP | − 580.5| 0.000   |
| (b) Response: Tensile strength ($S$) |
| Constant              | 34.364| 0.000   |
| wt% MWCNT             | 5.633 | 0.000   |
| wt% CSIMP             | − 1.423| 0.002   |
| wt% MWCNT × wt% MWCNT | − 2.132| 0.002   |
| wt% CSIMP × wt% CSIMP | − 2.059| 0.002   |
| wt% MWCNT × wt% CSIMP | − 7.935| 0.000   |
| (c) Response: fracture toughness ($K_{IC}$) |
| Constant              | 2.18200| 0.000   |
| wt% MWCNT             | 0.73826| 0.000   |
| wt% CSIMP             | 1.16762| 0.000   |
| wt% MWCNT × wt% MWCNT | − 0.36754| 0.000   |
| wt% CSIMP × wt% CSIMP | 0.09146| 0.425   |
| wt% MWCNT × wt% CSIMP | − 0.01181| 0.942   |

Table 3. Analysis of variance for the models and estimated regression coefficients. (a) R-Sq = 98.4%, R-Sq(adj) = 97.2%, P-value of Lack-of-Fit = 0.073, P-value of Regression = 0.000. R-Sq = 98.9%, R-Sq(adj) = 98.1%, P-value of Lack-of-Fit = 0.846, P-value of Regression = 0.000. (c) R-Sq = 98.2%, R-Sq(adj) = 97%, P-value of Lack-of-Fit = 0.113, P-value of Regression = 0.000.
toughness of host polymer by introducing restrictions to crack propagation and increasing the amount of plastic deformation. In other words, the propagating crack tips could not break the strong MWCNTs, and consequently, they force to arrest or change their directions. Also, the high magnification SEM fractograph of this specimen (Fig. 5c) shows a plethora of pulled-out nanotubes with curved pattern which indicate a great deal of difficulty in crack initiation and propagation within the matrix of MWCNT containing samples in comparison with bared epoxy matrix. Therefore, through the process of pulling out of MWCNTs from the epoxy matrix, a great deal of dissipation of energy has occurred which caused a remarkable amelioration in fracture toughness of the prepared nanocomposites.

It is well known that the dispersion state of MWCNTs could significantly affect the toughness and other physicomechanical properties of the epoxy polymer. Thus, it is expected that the observed agglomerations of MWCNTs in the fractograph of the binary composite (Fig. 5b) could act as weak and stress concentration areas and deteriorate physicomechanical properties of the epoxy polymer. By considering that such aggregated

Figure 4. Response surface and Contour plots of tensile properties and toughness of epoxy composites.
structures become more prevailing at the higher concentration of MWCNTs, it is plausible that the devastating effects of such conglomerations are more prominent at higher amounts of MWCNTs. Such phenomenon was observed as the deteriorative influence of MWCNTs on the $S$ and $K_{IC}$ of the epoxy composites at the Response surface and Contour plots in Fig. 4.

Figure 5d shows the fractograph of the binary composite of epoxy/CSIMPs. Rough fracture surface as well as spherical holes, which are related to the deboning of CSIMPs and subsequent plastic deformation of matrix indicate a ductile fracture of the prepared specimen. It is surmised that stress-activated shear yielding in the high-stress region around CSIMPs leads to the deformation of their rubbery portion and cavitation phenomenon, which in turn could significantly boost the toughness of epoxy resin. In addition, as it can be seen obviously, the sizes of the holes are considerably bigger than the measured size of CSIMPs in SEM images (Fig. 2). This observation is probably due to the massive plastic deformation of the matrix around the AIMPs.

Fractographs of toughened samples with MWCNTs and CSIMPs conspicuously show plastic deformation, crack deflection and pull-out MWCNTs (Fig. 5e,f). This observation surmised that a combination of crack deflection and inhibition of MWCNTs along with cavitation of CSIMPs could have synergistic toughening effects on the epoxy matrix and enhance its toughness remarkably. Also, it is observed that the conglomerations of MWCNTs at the ternary composite are considerably lower than MWCNTs/epoxy binary composite. As explained in Sect. 3.2, the probable explanation for such phenomenon could be due to the positive effect of CSIMPs on the dispersion state of MWCNTs.

**Conclusion**

In this study, for the first time CCD/RSM design was adopted to determine the optimum condition for tensile properties and fracture toughness of epoxy/MWCNT/CSIMPs ternary composite. The CCD/RSM prepared sufficient statistical data to fit a quadratic model in terms of the wt% MWCNTs and wt% CSIMPs in epoxy resin, on the tensile and toughness properties. The significance of the proposed models was indicated by the p-value of Regression < 0.0001 and P-value of LOF > 0.05. Analysis of variance showed good coefficient of determination values, $R^2$, (>98) for the studied properties. The optimum condition for maximum Young's modulus, tensile strength, and toughness of the epoxy composite obtained from RSM was 3 wt% MWCNTs and 1.03 wt% CSIMPs in the epoxy matrix. The sample prepared in optimal conditions indicated module = 3014 MPa, tensile strength = 40.57 MPa, and $K_{IC}$ = 2.2 MPa m$^{1/2}$. The obtained results indicated that the optimized ternary composites possess a good balance between Young's modulus, tensile strength, and toughness, which could not be achieved by other binary ones. The SEM images of the fractographs substantiated that combination of MWCNTs and CSIMPs could merge their toughening mechanisms and cause a synergistic toughening effect on the obtained ternary composite.
References
1. Gupta, S. K., Shukla, D. K. & Kaustubh, R. D. Effect of nanoalumina in epoxy adhesive on lap shear strength and fracture toughness of aluminium joints. J. Adhes. 97, 117–139 (2021).
2. Alfano, M. et al. Fracture toughness of structural adhesives for the automotive industry. Proc. Struct. Integra. 8, 561–565 (2018).
3. Hu, D. et al. Study on toughness improvement of a rosin-sourced epoxy matrix composite for green aerospace application. J. Compos. Sci. 4, 168 (2020).
4. Bain, E. D. et al. Failure processes governing high-rate impact resistance of epoxy resins filled with core–shell rubber nanoparticles. J. Mater. Sci. 51, 2347–2370 (2016).
5. Ha, S. R., Rhee, K. Y., Kim, H. C. & Kim, J. T. Fracture performance of clay/epoxy nanocomposites with clay surface-modified using 3-aminopropyltriethoxysilane. Colloids Surf. A Physicochem. Eng. Asp. 313, 112–115 (2008).
6. Johnsen, B. B., Kinloch, A. J., Mohammed, R. D., Taylor, A. C. & Sprenger, S. Toughening mechanisms of nanoparticle-modified epoxy polymers. Polymer 48, 530–541. https://doi.org/10.1016/j.polymer.2006.11.038 (2007).
7. Zhang, X., Xu, W., Xia, X., Zhang, Z. & Yu, R. Toughening of cycloaliphatic epoxy resin by nanosize silicon dioxide. Mater. Lett. 60, 3319–3323 (2006).
8. Chen, J., Kinloch, A. J., Sprenger, S. & Taylor, A. C. The mechanical properties and toughening mechanisms of an epoxy polymer modified with polysiloxane-based core-shell particles. Polymer (Guildf) 54, 4276–4289 (2013).
9. Tsang, W. L. & Taylor, A. C. Fracture and toughening mechanisms of silica- and core–shell rubber-toughened epoxy at ambient and low temperature. J. Mater. Sci. 54, 13938–13958 (2019).
10. Dittanet, P. & Pearson, R. A. Effect of silica nanoparticle size on toughening mechanisms of filled epoxy. Polymer (Guildf) 53, 1890–1905. https://doi.org/10.1016/j.polymer.2012.02.052 (2012).
11. Bakar, M., Bialkowska, A., Kuritka, I., Hanulikova, B. & Masaj, M. Synergistic effects of thermoplastic and nanoclay on the performance properties and morphology of epoxy resin. Polym. Compos. 39, E2540–E2551 (2018).
12. Wang, J. et al. Synergistically effects of copolymer and core–shell particles for toughening epoxy. Polymer (Guildf) 140, 39–46 (2018).
13. Liang, Y. L. & Pearson, R. A. The toughening mechanism in hybrid epoxy-silica-rubber nanocomposites (HESRNPs). Polymer (Guildf) 51, 4880–4890 (2010).
14. Li, T., He, S., Stein, A., Francis, L. F. & Bates, F. S. Synergistic toughening of epoxy modified by graphene and block copolymer micelles. Macromolecules 49, 9507–9520 (2016).
15. Ricciardi, M. R. et al. Mechanical properties of glass fibre composites based on nitrile rubber toughened modified epoxy resin. Compos. Part B Eng. 139, 259–267 (2018).
16. Hsieh, T. H. et al. The toughness of epoxy polymers and fibre composites modified with rubber microparticles and silica nanoparticles. J. Mater. Sci. 45, 1193–1210 (2010).
17. Imtiaz, S. et al. A review featuring fabrication, properties and applications of carbon nanotubes (CNTs) reinforced polymer and epoxy nanocomposites. Chin. J. Polym. Sci. 36, 445–461 (2018).
18. Gómez-del Río, R., Salazar, A., Pearson, R. A. & Rodriguez, J. Fracture behaviour of epoxy nanocomposites modified with triblock copolymers and carbon nanotubes. Compos. Part B Eng. 87, 343–349 (2016).
19. Schuster, M. B., Oppelt, C. V., Becker, D. & Coello, L. A. F. Role and synergy of block copolymer and carbon nanotubes on toughness in epoxy matrix. Polym. Compos. 39, E2262–E2273 (2018).
20. Rahim-Abadi, M. M., Mahdavian, A. R., Gharieh, A. & Salehi-Mobarakeh, H. Chemical modification of TiO₂ nanoparticles as an effective way for encapsulation in polyacrylic shell via emulsion polymerization. Prog. Org. Coat. 88, 310–315. https://doi.org/10.1016/j.porgcoat.2015.07.013 (2015).
21. Song, H., Chung, H. & Nam, K. Response surface modeling with Box–Behnken design for strontium removal from soil by calcium-based solution. Environ. Pollut. 274, 116577 (2021).
22. Dorraji, M. S. S., Rasoulofard, M. H., Khorasani, F. M., Rezaee, G. H., Zarrabi, A. & Barzegar, H. K. Microwave absorption properties of polyaniline-Fe₃O₄/ZnO-polyester nanocomposite: Preparation and optimization. Appl. Surf. Sci. 366, 210–218 (2016).
23. Gharieh, A., Khoei, S. & Mahdavian, A. R. Emulsion and miniemulsion techniques in preparation of epoxy nanoparticles with versatile characteristics. Adv. Colloid Interface Sci. 269, 152–186. https://doi.org/10.1016/j.cis.2019.04.010 (2019).
24. Bovier Fontes, L., Pirri, R., Asua, J. M. & Leiza, J. R. Cross-linking emulsion copolymerization of butyl acrylate with diallyl maleate. J. Polym. Sci. Part A Polym. Chem. 43, 4684–4694 (2005).
25. Gharieh, A., Mahdavian, A. R. & Salehi-Mobarakeh, H. Preparation of core-shell impact modifier particles for PVC with nanometric shell thickness through seeded emulsion polymerization. Iran. Polym. J. (English Ed.) 23, 27–35. https://doi.org/10.1007/s13726-013-0196-5 (2014).
26. Guild, F. J., Kinloch, A. J. & Taylor, A. C. Particle cavitation in rubber toughened epoxies: The role of particle size. J. Mater. Sci. 45, 3882–3894 (2010).
27. Kim, D. S., Cho, K., Kim, J. K. & Park, C. E. Effects of particle size and rubber content on fracture toughness in rubber-modified epoxies. Polym. Eng. Sci. 36, 755–768 (1996).
28. Bajpai, A., Wetzel, B., Klinger, A. & Friedrich, K. Mechanical properties and fracture behavior of high-performance epoxy nanocomposites modified with block polymer and core–shell rubber particles. J. Appl. Polym. Sci. 137, 48471 (2020).
29. Gharieh, A., Moghadam, M. & Pourhasem, M. Synergistic effects of acrylic/silica armored structured nanoparticles on the toughness and physomechanical properties of epoxy polymers. ACS Appl. Polym. Mater. 3, 4008–4016 (2021).
30. Wu, G., Zhao, J., Shi, H. & Zhang, H. The influence of core–shell structured modifiers on the toughness of poly (vinyl chloride). Eur. Polym. J. 40, 2451–2454 (2004).
31. Tkachenko, V. et al. A DSC and XPS characterization of core–shell morphology of block copolymer nanoparticles. Colloid Polym. Sci. 298, 1095–1105 (2020).
32. Gojny, F. H., Wichmann, M. H. G., Köpke, U., Fiedler, B. & Schulte, K. Carbon nanotube-reinforced epoxy-composites: Enhanced stiffness and fracture toughness at low nanotube content. Compos. Sci. Technol. 64, 2363–2371 (2004).
33. Giannakopoulos, G., Masania, K. & Taylor, A. C. Toughening of epoxy using core–shell particles. J. Mater. Sci. 46, 327–338 (2011).
34. Mirmohseni, A., Gharieh, A. & Khorasani, M. Silica encapsulation by miniemulsion polymerization: A novel approach of efficient chemical functionalization on silica nanoparticles. Polymer (Guildf) 98, 182–189. https://doi.org/10.1016/j.polymer.2016.06.035 (2016).
35. Ren, X. et al. Critical rubber layer thickness of core-shell nanoparticles with a rigid core and a soft shell for toughening of epoxy resins without loss of elastic modulus and strength. Compos. Sci. Technol. 153, 253–260 (2017).
36. Pothen, J. R., Kalvanyasundaram, D. & Gururaja, S. Enhancement of open hole tensile strength via alignment of carbon nanotubes infused in glass fiber–epoxy-CNT multicomposite composites. Compos. Part A Appl. Sci. Manuf. 140, 106155 (2021).
37. Quan, D. & Ivanovskii, A. Effect of core–shell rubber (CSR) nano-particles on mechanical properties and fracture toughness of an epoxy polymer. Polymer (Guildf) 66, 16–28 (2015).

Received: 25 May 2021; Accepted: 11 October 2021
Published online: 21 October 2021
38. Rafiee, M., Nitzsche, F. & Labrosse, M. R. Effect of functionalization of carbon nanotubes on vibration and damping characteristics of epoxy nanocomposites. Polym. Test 69, 385–395 (2018).
39. Tang, L.-C. et al. Fracture toughness and electrical conductivity of epoxy composites filled with carbon nanotubes and spherical particles. Compos. Part A Appl. Sci. Manuf. 45, 95–101 (2013).
40. Xu, C. et al. Enhanced toughness and thermal conductivity for epoxy resin with a core–shell structured polyacrylic modifier and modified boron nitride. RSC Adv. 9, 8654–8663 (2019).
41. Jaafar, C. N. A., Zainol, I., Ishak, N. S., Ilyas, R. A. & Sapuan, S. M. Effects of the liquid natural rubber (LNR) on mechanical properties and microstructure of epoxy/silica/kenaf hybrid composite for potential automotive applications. J. Mater. Res. Technol. 12, 1026–1038 (2021).

Author contributions
The authors contributed in the following ways: A.G., supervision, conceptualization, writing, review, and editing; M.S.S.D. experiments and analyses.

Competing interests
The authors declare no competing interests.

Additional information
Correspondence and requests for materials should be addressed to A.G.

Reprints and permissions information is available at www.nature.com/reprints.

Publisher’s note Springer Nature remains neutral with regard to jurisdictional claims in published maps and institutional affiliations.

Open Access This article is licensed under a Creative Commons Attribution 4.0 International License, which permits use, sharing, adaptation, distribution and reproduction in any medium or format, as long as you give appropriate credit to the original author(s) and the source, provide a link to the Creative Commons licence, and indicate if changes were made. The images or other third party material in this article are included in the article’s Creative Commons licence, unless indicated otherwise in a credit line to the material. If material is not included in the article’s Creative Commons licence and your intended use is not permitted by statutory regulation or exceeds the permitted use, you will need to obtain permission directly from the copyright holder. To view a copy of this licence, visit http://creativecommons.org/licenses/by/4.0/.

© The Author(s) 2021