Ab Initio Study of the Large Amplitude Motions of Various Monosubstituted Isotopologues of Methylamine (CH$_3$-NH$_2$)

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CCSD(T)-F12 theory is applied to determine electronic ground state spectroscopic parameters of various isotopologues of methylamine (CH$_3$-NH$_2$) containing cosmological abundant elements, such as D, $^{13}$C and $^{15}$N. Special attention is given to the far infrared region. The studied isotopologues can be classified in the G$_{12}$, G$_6$ and G$_4$ molecular symmetry groups. The rotational and centrifugal distortion constants and the anharmonic fundamentals are determined using second order perturbation theory. Fermi displacements of the vibrational bands are predicted. The low vibrational energy levels corresponding to the large amplitude motions are determine variationally using a flexible three-dimensional model depending on the NH$_2$ bending and wagging and the CH$_3$ torsional coordinates. The model has been defined assuming that, in the amine group, the bending and the wagging modes interact strongly. The vibrational levels split into six components corresponding to the six minima of the potential energy surface. The accuracy of the kinetic energy parameters has an important effect on the energies. Strong interactions among the large amplitude motions are observed. Isotopic effects are relevant for the deuterated species.

Keywords: methylamine, LAM, torsion, wagging, $^{13}$CH$_3$NH$_2$, CH$_3$$^{15}$NH$_2$, CH$_3$NHD, CH$_2$DNH$_2$

INTRODUCTION

Methylamine (CH$_3$-NH$_2$) plays important roles in the gas phase chemistry in the terrestrial and extraterrestrial atmospheres. The presence in the Earth’s atmosphere has both natural and anthropogenic causes (Ge et al., 2011). In air quality studies, it is considered to be a Volatile Organic Compound (VOC) that can be a precursor of secondary organic aerosols (SOA) in the presence of glyoxal (De Haan et al., 2009). In 1974, it was detected in the interstellar medium and it is contemplated as a relatively abundant species (Kaifu et al., 1974) (Fourikis et al., 1974). Recent studies consider it a precursor of glycine and a building block of life (Ohoshi et al., 2019). Recently, methylamine has been detected in the quasar PKS 1830-211 (Muller et al., 2011) and together with other simple N-bearing species, it has been observed in the hot cores NGC 6334I MM1-3 (Bøgelund et al., 2019). Fourikis et al. (1977) have reported the probable detection of deuterated methylamine (CH$_3$NHD) in Sgr B2.

The aim of the present work is the theoretical study of probably detectable methylamine isotopologues. Monosubstituted isotopologues were detected for many astrophysical molecules such as dimethyl-ether and methyl-formate as it is described in the references provided by the papers.
of Fernández et al. (2019) and Gámez et al. (2019). In a recent study of the methylamine main isotopologue, highly correlated ab initio methods were employed to simulate the far infrared spectra (Senent 2018). The low-lying vibrational energy levels in and their tunneling splitting components were computed, providing relevant information for rotational spectrum assignments, which are mandatory for the detection using radio-astronomy. Very accurate results were obtained by comparing with previous experimental data. A detailed review of previous theoretical and experimental works can be found in Senent (2018).

The motivation of many previous studies of methylamine concerns more to the peculiar molecular structure than to its molecule where two interacting large amplitude motions, the torsion of the methyl group and the NH2 wagging, govern its internal dynamics (Ohashi & Hougen 1987) (Kreglewski 1978, 1989) (Ohashi & Toriyama 1994 (Kleiner and Hougen, 2015). High resolution rovibrational spectra have been measured for the ground and various excited vibrational states, given a special attention to the far infrared region (Belorgeot et al., 1982) (Diallo et al., 1985) (Ohashi et al., 1987, 1988, 1989, 1992) (Ilyushin et al., 2005) (Kreglewski & Winther 1992) (Kreglewski & Wlodarczak 1992) (Motiyenko et al., 2014) (Nguyen et al., 2021) (Dawadi et al., 2013a; 2013b).

Whereas publications about the methylamine main isotopologue are recurrent, less studies attend to other isotopic species. The microwave spectrum of the monosubstituted species CH3NHD (Ohashi et al., 1991), CH3DNH2 (Tamagake & Tsuboi 1974), and 13CH2NH2 (Motiyenko et al., 2016), and the deuterated species, CH3ND2, CD2NH2, CD3ND2 (Lide 1954) (Sastry 1960) (Takagi & Kojima 1971) (Kreglewski et al., 1990a; 1990b) were measured and assigned. The infrared absorption spectrum of 15N-methylamine was inspected in the gas phase (Hirakawa et al., 1972). Mass resolved excitation spectroscopy and ab initio calculations were employed to analyze the low-lying excited states of CH2NH2, CH2NH2, CD2NH2, CH3ND2, and CD3ND2 (Taylor & Bernstein 1995). The A→X excitation spectra of six different deuterated isotopologues including the CH3NHD monosubstituted species, were explored (Park et al., 2006).

Previous studies devoted to n-methyl amines describe theoretical techniques and symmetry concepts useful for the present work (Senent & Smyers 1996) (Smyers et al., 1996, 1998) (Senent 2018). On the basis of previous ab initio results (Senent 2018), performed using explicitly correlated coupled cluster theory, CCSD(T)-F12 (Adlet et al., 2007) (Knizia et al., 2009) using the MOLPRO package default fitting and the resolutions of the identity. These previous computed data are mass independent properties that can be used for the different isotopic species.

To determine the core-valence electron correlation effects on the rotational constants, the structure was optimized using CCSD(T) (coupled-cluster theory with single and double substitutions, augmented by a perturbative treatment of triple excitations (CCSD(T)-F12b) (Adlet et al., 2007) (Knizia et al., 2009) using the MOLPRO package default setting and the resolutions of the identity. These previous computed data are mass independent properties that can be used for the different isotopic species.

An earliest CCSD(T)-F12 three-dimensional potential energy surface is revisited in the present work (Senent 2018) because it is mass independent. It is employed for constructing mass dependent effective potential energy surfaces for the different isotopologues. The surfaces present six minima separated by relatively low potential energy barriers. If the minimum interconversion is taken into consideration, the most abundant isotopologue can be classified in the G12 molecular symmetry group (Ohashi & Hougen 1987). The isotopic substitutions carry out changes in the symmetry. Details concerning the followed procedure can be found in our previous paper devoted to the acetone isotopologues (Dalbouha et al., 2021). The effective surfaces allow to construct Hamiltonians depending on three interacting coordinates, two interacting large amplitude motions, the NH2 wagging and the CH3 torsion, and the HNH bending. Then, both the bending and wagging of the amine group are treated together. The final levels are computed variationally.

RESULTS AND DISCUSSION

Electronic Structure Calculations

The theoretical study of methylamine isotopologues was started from the results of a previous work devoted to the main isotopologue CH3NH2 (Senent 2018). In this earlier paper, the structural parameters of the minimum energy structure and a three-dimensional ab initio potential energy surface (3D-PES) were computed using explicitly correlated coupled cluster theory with single and double substitutions augmented by a perturbative treatment of triple excitations (CCSD(T)-F12b) (Adlet et al., 2007) (Knizia et al., 2009) using the MOLPRO package default setting (Werner et al., 2012). The procedure was applied in connection with the AVTZ-F12 basis set, which contains the Dunning's type aug-cc-pVTZ atomic orbitals (AVTZ) (Kendall et al., 1992) and the corresponding functions for the density fitting and the resolutions of the identity. These previous computed data are mass independent properties that can be used for the different isotopic species.

To determine the core-valence electron correlation effects on the rotational constants, the structure was optimized using CCSD(T) (coupled-cluster theory with single and double substitutions, augmented by a perturbative treatment of triple excitations) (Hampel et al., 1992) and the cc-pCVTZ basis set (CVTZ) (Woon and Dunning Jr 1995).

The full-dimensional anharmonic force field and the vibrational corrections of the potential energy surface are mass dependent properties that must be computed for each isotopologue. For this reason, new electronic structure calculations have been performed in the present work. That properties were determined using second order Möller-Plesset theory (MP2) (Moller & Plesset 1934) implemented in GAUSSIAN (Frisch et al., 2016). Anharmonic force fields allow obtain spectroscopic properties using second order perturbation theory (VPT2) (Barone 2005) (Bloino et al., 2012). The vibrationally corrected surfaces were employed to construct Hamiltonians for the isotopologues. The energy levels corresponding to the large amplitude vibrations and to the HNH
bending mode were computed using a variational procedure implemented in ENEDIM (Senent 1998a; 1998b, 2001).

### The Symmetry of the Isotopologues

The main isotopologue, as well as $^{13}$CH$_3$NH$_2$ and CH$_3^{15}$NH$_2$, can be classified in the $G_{12}$ molecular symmetry group (MSG) (Ohashi & Hougen 1987) and in the C$_1$ point group. However, the $H \rightarrow D$ substitution carries out changes in the symmetry properties. CH$_3$NDH must be classified in the C$_1$ point group and in the $G_6$ MSG, due to the absence of the symmetry plane. In CD$_3$NH$_2$, the D atom can replace the in-plane H atom (C$_{2}$-CDH$_2$NH$_2$) or one out-of-plane H atom (C$_{1}$-CDH$_2$NH$_2$). If VPT2 is applied and a unique minimum is considered, the molecule is assumed to be semi-rigid and all the vibrations are described as small displacements around the equilibrium. Two different point groups C$_1$ and C$_3$ are used. However, if the internal rotation is taken into account, C$_{2}$-CDH$_2$NH$_2$ and C$_{1}$-CDH$_2$NH$_2$ represent different minima of the same potential energy surface and they can be inter-converted. Then, both are classified in the same $G_4$ MSG.

The $G_{12}$ MSG contains six irreducible representations, four non-degenerate, A$_1$, A$_2$, B$_1$, and B$_2$, and two double-degenerate E$_1$ and E$_2$. The $G_6$ MSG contains three irreducible representations, two non-degenerate, A$_1$, and A$_2$, and one double-degenerate E. The $G_4$ MSG contains four non-degenerate irreducible representations, A$_1$, A$_2$, B$_1$, and B$_2$.

### Rovibrational Parameters

In the earlier paper (Senent 2018), the CCSD(T)-F12/AVTZ structural parameters of the methylamine equilibrium geometry, are detailed. The structure is shown in Figure 1, that helps to understand the atom labelling and the isotopic substitutions.

For all the isotopologues, the vibrational ground state rotational constants shown in Table 1, were computed from the CCSD(T)-F12 equilibrium rotational constants using the following equation:

$$B_0 = B_e (\text{CCSD(T)} - \text{F12/AVTZ} - \text{F12}) + \Delta B_e^{\text{core}} (\text{CCSD(T)/CVTZ}) + \Delta B_e^{\text{ab}} (\text{MP2/AVTZ})$$

(1)

Here, $\Delta B_e^{\text{core}}$ collects the core-valence electron correlation effects on the equilibrium structure and $\Delta B_e^{\text{ab}}$ represents the vibrational contribution derived from the second order perturbation theory (VPT2) $\alpha_\nu$ vibration-rotation interaction parameters. These last were determined using the MP2/AVTZ cubic force fields and vibrational second order perturbation theory. $\Delta B_e^{\text{core}}$ was determined from the CCSD(T)/CVTZ parameters $B_e$ (CV) and $B_e$ (V), calculated correlating both core and valence electrons (CV) or just the valence electrons (V) in the post-SCF process. Then:

$$\Delta B_e^{\text{core}} = B_e (\text{CV}) - B_e (\text{V})$$

(2)

This approximation has been corroborated in previous studies of other non-rigid molecules providing really accurate parameters, whose deviations with respect available experimental data, represent few MHz (Boussesi et al., 2016) (Dalbouha et al., 2016, 2021). In Table 1, the computed rotational constants of CH$_3$NH$_2$, $^{13}$CH$_3$NH$_2$, and CH$_3$NDH are compared with available experimental parameters (Ilyushin et al., 2005) (Motiyenko et al., 2016) (Ohashi et al., 1991). The MP2/AVTZ quartic centrifugal distortion constants corresponding to the asymmetrically reduced Hamiltonian, are shown in Table 2 where they are compared with previous experimental data (Ilyushin et al., 2005) (Motiyenko et al., 2016) (Ohashi et al., 1991). Disagreements between experimental and computed data can be correlated with the level of ab initio calculations used to compute the anharmonic force field. In addition, in methyl amine, the interaction between the internal and global rotation causes deviations. Isotopic shifts are more reliable.

The anharmonic fundamental frequencies shown in Table 3, were computed using VPT2 theory (Barone 2005) (Blöino et al., 2012) implemented in Gaussian (Frisch et al., 2016) and the MP2/AVTZ force fields. The modes are ordered following the criteria used for the main isotopologue that helps to make visible the isotopic shifts. Although VPT2 does not represent the proper treatment for the study of the vibrations responsible for the non-rigidity, it provides a good description of the mid- and near-infrared regions and a useful first description of the far-infrared region. In addition, it allows predict possible band displacements due to Fermi resonances. VPT2 theory ignores the inter-conversion of minima and treats the molecule as a semi-rigid species with a single minimum. If the existence of a single minimum is assumed, the resulting VPT2 frequencies are different for C$_{2}$-CDH$_2$NH$_2$ than for C$_{1}$-CDH$_2$NH$_2$.

The frequencies corresponding to the main isotopologue are compared with experimental data measured in the gas phase (Ohashi et al., 1989) (Kreglewski & Włodarczak 1992) (Gulaczyk et al., 2017) (Hirakawa et al., 1972) [58]. Previous results are available for CH$_3^{15}$NH$_2$ (Hirakawa et al., 1972). Deviation for several modes are significant, whereas the isotopic shifts computed at the MP2 level of theory are reliable.
In Table 3, emphasized in bold, are the fundamental frequencies for which resonances can be relevant. Displacements due to the Fermi interactions were found to be relevant for the $\nu_3$ fundamental (CH$_3$ st), that interacts with two overtones (2$\nu_6$ and 2$\nu_{12}$). The NH$_2$ bending fundamental is predicted to interact strongly with the NH$_2$ wagging overtone. Since both amine vibrations behave as inseparable modes, the variational model used for exploring the far infrared region, includes explicitly the bending coordinate.

The far Infrared Spectrum
As was assumed in the previous paper devoted to the main isotopologue (Senent 2018), the low-lying vibrational energy levels corresponding to the two large amplitude motions, the methyl torsion ($\theta$) and the amine NH$_2$ wagging ($\alpha$) can be determined by solving variationally a three-dimensional Hamiltonian where a third coordinate, the HNH bending angle ($\beta$), is considered to be an independent variable. The Hamiltonian obeys the formula:

$$H(\beta, \alpha, \theta) = -\sum_{i=1}^{3} \sum_{j=1}^{3} \left( \frac{\partial}{\partial \beta_i} \right) B_{ij}(\beta, \alpha, \theta) \left( \frac{\partial}{\partial \beta_j} \right) + V_{eff}(\beta, \alpha, \theta)$$

(3)

This Hamiltonian was defined by taking into consideration the predictions of the test of resonances described in the previous section and in the previous paper (Senent 2018). Significant interactions between the NH$_2$ bending and wagging vibrational modes were predicted. This fact suggests the prerequisite of a 3D-model. In Eq. 3, $B_{ij}(\beta, \alpha, \theta)$ and $V_{eff}(\beta, \alpha, \theta)$ represent the kinetic energy parameters and the effective potential defined as the sum of three contributions:

$$V_{eff}(\beta, \alpha, \theta) = V(\beta, \alpha, \theta) + V'(\beta, \alpha, \theta) + V_{ZPVE}(\beta, \alpha, \theta)$$

(4)

Here, $V(\beta, \alpha, \theta)$ is the mass independent ab initio three-dimensional potential energy surface; $V'(\beta, \alpha, \theta)$ and $V_{ZPVE}(\beta, \alpha, \theta)$ represent the Podolsky pseudopotential and the zero point vibrational energy correction (Dalbouha et al., 2021).
The two last contributions must be computed for all the isotopologues because they are mass dependent properties. \( \beta \), \( \alpha \), and \( \theta \), the HNH bending, the NH2 wagging and the torsional coordinates, are defined using curvilinear internal coordinates:

\[
\begin{align*}
\beta &= \text{HNH} - \text{HNH}^e \\
\alpha &= 180.0 - \gamma \\
\theta &= \frac{(H5C4N1X + H6C4N1X + H7C4N1X - 2\Pi)}{3} \\
\end{align*}
\]  

(5)

\( \text{HNH}^e \) is the value of the HNH bending angle corresponding to the equilibrium geometry; \( \gamma \) represents the angle between the C-N bond and the HNH plane (see Figure 1); \( X \) denotes a ghost atom lying in the HNH plane perpendicular to the HNH angle bisector. The set of internal coordinates were chosen taking into consideration the procedure for the determination of the 3D-PES which demands a partial optimization of the geometry. Three internal coordinates, NHN, \( \gamma \) and H5C4N1X distinguish the selected conformations whereas twelve “dependent coordinates” are allowed to be relaxed in all the structures.

The ab initio three-dimensional potential energy surface, \( V(\beta, \alpha, \theta) \), was computed for the study of the main isotopologue (Senent 2018). It was constructed using the CCSD(T)-F12/AVTZ energies of 131 geometries defined for selected values of the independent coordinates that were fitted to the following series:

| Mode | assign. | Senent (2018) | Shimanouchi (1972) | This work | This work | Hirakawa et al., 1972 |
|------|---------|---------------|---------------------|-----------|-----------|-------------------------|
| 1    | NH2 st  | 3,388         | 3,361               | 3,385     | 3,380     | 3,354.5                 |
| 2    | CH3 st  | 3,001         | 2,961               | 2,989     | 3,010     | 2,961.2                 |
| 3    | CH3 st  | 2,931         | 2,820               | 2,909     | 2,916     | 2,820                   |
| 4    | NH2 b   | 1,610         | 1,623               | 1,639     | 1,635     | 1,618.7                 |
| 5    | CH3 b   | 1,481         | 1,473               | 1,476     | 1,478     | 1,473.6                 |
| 6    | CH3 b   | 1,453         | 1,430               | 1,426     | 1,433     | 1,430.4                 |
| 7    | HCN b   | 1,146         | 1,130               | 1,127     | 1,131     | 1,126.2                 |
| 8    | NC st   | 1,055         | 1,044               | 1,032     | 1,037     | 1,031.7                 |
| 9    | NH3 wag | 781           | 780                 | 787       | 783       | 775.8                   |
| 10   | NH3 st  | 3,464         | 3,427               | 3,462     | 3,453     | 3,415                   |
| 11   | CH3 st  | 3,034         | 2,986               | 3,021     | 3,031     | 2,985                   |
| 12   | CH3 b   | 1,481         | 1485c               | 1,495     | 1,495     | 1,485                   |
| 13   | HNC b   | 1,315         | 1,292               | 1,296     |           |                         |
| 14   | CH3 b   | 971           | 965                 | 966       |           |                         |
| 15   | CH3 tor | 288           | 268                 | 274       | 274       |                         |

| CH3NDH | Cs-CD3NH3/C1-CD3NH2 |
|---------|---------------------|
| mode    | assign. | This work | This work |
| 1       | NH2 st  | 2,528     | 3,384/3,385 |
| 2       | CH3 st  | 3,000     | 2,998/2,898 |
| 3       | CH3 st  | 2,915     | 2,160/2,228 |
| 4       | NH2 b   | 1,461     | 1,605/1,654 |
| 5       | CH3 b   | 1,478     | 1,458/1,476 |
| 6       | CH3 b   | 1,432     | 1,337/1,324 |
| 7       | HCN b   | 1,152     | 1,078/1,062 |
| 8       | NC st   | 1,038     | 920/1,046 |
| 9       | NH2 wag | 691       | 767/780 |
| 10      | NH2 st  | 3,422     | 3,462/3,462 |
| 11      | CH3 st  | 3,032     | 3,025/3,010 |
| 12      | CH3 b   | 1,496     | 1,373/1,356 |
| 13      | HNC b   | 1,219     | 1,246/1,228 |
| 14      | CH3 b   | 878       | 937/845 |
| 15      | CH3 tor | 247       | 265/262 |

a) Emphasized in bold the transitions displaced by Fermi resonances.
b) st = stretching; b = bending; w = wagging; tor = torsion.
c) Hirakawa et al., 1972; d) Ohashi et al., 1988; e) Kreglewski & Wlodarczak 1992; f) Gulaczyk et al., 2017.
This analytical expression transforms as the totally symmetric representation of the G12 MSG. Formally identical expressions can be employed for \( V', V_{ZPVE}, V_{\text{eff}}(\beta, \alpha, \theta) \) and the diagonal kinetic energy parameters \( B_{\text{qiqj}} \) of the main isotopologue, \(^{13}\text{CH}_3\text{NH}_2\) and \( \text{CH}_3^{15}\text{NH}_2 \). However, since the H \( \rightarrow \) D substitution carries out symmetry changes, the effective potential \( V_{\text{eff}}(\beta, \alpha, \theta) \) and the diagonal kinetic parameters must be expressed using less-symmetric analytical expressions. For \( \text{CH}_3\text{NDH} \) (G6):

\[
V_{\text{eff}}(\beta, \alpha, \theta) = \sum_{K,L,M} A_{KLM}^{CC} \beta^K \cos L \alpha \cos 3M \theta + A_{KLM}^{SS} \beta^K \sin L \alpha \sin 3(2M + 1)\theta \tag{6}
\]

\[
V_{\text{eff}}(\beta, \alpha, \theta) = \sum_{K,L,M} A_{KLM}^{CC} \beta^K \cos L \alpha \cos 3M \theta + A_{KLM}^{SS} \beta^K \sin L \alpha \sin 3M \theta \tag{7}
\]
TABLE 4 | CCSD(T)-F12/AVTZ potential energy barriers (in cm⁻¹).

|                  | CH₃-NH₂ | ¹⁴CH₃-NH₂ | CH₃-¹⁵NH₂ | CH₃-NDH | CDH₂-NH₂ |
|------------------|---------|-----------|-----------|---------|----------|
|                  | This work | Previous works | This work | This work | This work | This work |
| Vₐff             | 703      | 684.71(1) ¹⁺ 681.05(1) ²⁺ 714.55(1) ³⁺ |
|                  | 1907     | 1927      | 1926      | 1890    | 1907     |
| Aₓₓₓₓ(Boh)        | 34.8345  | 34.8021   | 34.7823   | 25.9961 | 35.1168  |
| Aₓₓₓₓ(Boω)        | 24.9448  | 24.9168   | 24.7859   | 26.8749 | 20.3891  |
| Aₓₓₓₓ(Boө)        | 19.0289  | 19.0349   | 19.1537   | 19.4989 | 20.7992  |
| Aₓₓₓₓ(Boө)        | 0.00     | 15.1130   | 24.7859   | 19.4989 | 20.7992  |

a) Ohashi et al., 1988; b) Ohashi et al., 1992; c) Kreglewski 1993.

and for CDH₂NH₂ (G₄)

\[ V_{\text{eff}} (\beta, \alpha, \theta) = \sum_{KLM} A_{KML}^{\text{CC}} \cos La \cos 2M\theta + A_{KML}^{\text{SE}} \sin L\alpha \sin (2M + 1)\theta \]  

(8)

TABLE 5 | Symmetry eigenvectors.

|                  |                  |                  |
|------------------|------------------|------------------|
|                  | G₁₄              | A₁               |
|                  |                  |                  |
|                  | Xₖ cos (La) cos6Mθ | Xₖ sin (La) sin6M + 3θ |
|                  | Xₖ cos (La) sin6Mθ | Xₖ sin (La) sin6M - 2θ |
|                  |                  |                  |
|                  | B₁               |                  |
|                  |                  |                  |
|                  | Xₖ cos (La) cos6Mθ | Xₖ sin (La) sin6M + 3θ |
|                  | Xₖ cos (La) sin6Mθ | Xₖ sin (La) sin6M - 2θ |
|                  |                  |                  |
|                  | B₂               |                  |
|                  |                  |                  |
|                  | Xₖ cos (La) cos6Mθ | Xₖ sin (La) sin6M + 3θ |
|                  | Xₖ cos (La) sin6Mθ | Xₖ sin (La) sin6M - 2θ |
|                  |                  |                  |
|                  | A₂               |                  |
|                  |                  |                  |
|                  | Xₖ cos (La) cos6Mθ | Xₖ sin (La) sin6M + 3θ |
|                  | Xₖ cos (La) sin6Mθ | Xₖ sin (La) sin6M - 2θ |
|                  |                  |                  |
|                  | G₆               |                  |
|                  |                  |                  |
|                  |                  |                  |
|                  |                  |                  |
|                  |                  |                  |
|                  |                  |                  |
|                  |                  |                  |
|                  |                  |                  |
|                  |                  |                  |

To construct the effective potential using Eq. 4, two mass-dependent properties V' and V'eff must be computed for all the isotopologues and for all the geometries. The V' pseudopotential is very small. However, V'eff has important effects on the levels. It was determined within the harmonic approximation at the MP2/AVTZ level of theory. To obtain the mass-dependent properties of the low-symmetry varieties, more than 131 geometries and more than 131 sets of harmonic frequencies need to be computed. For example, in the case of CDH₂NH₂, 131x3 geometries are required because the three hydrogen atoms of the methyl group are not identical.

The ground vibrational state potential energy surface contains six equivalent minima corresponding to a single conformer. The contours of Figures 2, 3 represents layers of the 3D-surface of the main isotopologue containing the minimum energy structure. Figure 2 corresponds to Veff (α, β; θ = 270°) and Figure 3 to Veff (α, θ; β = 106°). Figures emphasize the coupling between coordinates.

The kinetic energy parameters were also computed for all the selected geometries and for all the isotopologues. The number of selected geometries required for their computation in the deuterated forms was 171 and 393 for CH₃NDH and CDH₂NH₂, respectively. For all the symmetries, the diagonal terms Bββ, Bωω, and Bөө transform as the totally symmetric representation A₁. However, the symmetry properties of the off-diagonal elements vary with the MSG:

Bββ transforms as B₁ (G₁₂, G₄) and A₁ (G₆)
Bωω transforms as B₂ (G₁₂, G₄) and A₂ (G₆)
Bөө transforms as A₂ (G₁₂, G₄, G₆)

The non-zero coefficients A₀₀₀(B₀₁₀) of the kinetic energy expressions are shown in Table 4. For the main isotopologue, they are compared with previous data (Ohashi et al., 1988, 1992), although in works based in experiments, these coefficients are considered to be constants. The potential energy barriers, V'eff and V'eff were estimated using the effective potentials. For the main isotopologue, they are in reasonable good agreement with previous data (Ohashi et al., 1988, 1992) (Kreglewski 1993). Isotopic shifts of all the potential parameters are only important for the deuterated forms.

Symmetry adapted series were employed as trial functions for the variational calculations. Products of harmonic oscillator solutions Xₖ (for the bending coordinate) and double Fourier series (for the wagging and torsional coordinates) were employed. Table 5 shows...
| $\tilde{v}_{\text{NN}}$-7,8,15 | CH$_3$NH$_2$ (G$_{12}$) | $^{15}$CH$_3$NH$_2$ (G$_{12}$) | CH$_2$-$^{15}$NH$_2$ (G$_{12}$) | CH$_2$-NDH (G$_4$) | CDH$_2$-NH$_2$ (G$_4$) |
|---|---|---|---|---|---|
| This work | Kreglewski (1989) | This work | |
| 0 0 0 | A$_1$ | 0.000 | 0.000 | 0.000 | A$_1$ | 0.000 |
| | B$_2$ | 0.163 | 0.078 | 0.167 | A$_2$ | 0.071 |
| | E$_1$ | 0.325 | 0.263 | 0.028 | E | 0.117 |
| | E$_2$ | 0.407 | 0.338 | 0.412 | E | 0.398 |
| 0 0 1 | B$_1$ | 265.572 | 269.88 | 264.441 | A$_1$ | 236.260 |
| | A$_2$ | 266.117 | 270.20 | 264.995 | A$_2$ | 236.470 |
| | E$_1$ | 259.316 | 260.94 | 258.241 | E | 233.571 |
| | E$_2$ | 259.066 | 261.18 | 257.987 | E | 233.571 |
| 0 0 2 | A$_1$ | 447.074 | 419.47 | 446.642 | A$_1$ | 416.671 |
| | B$_2$ | 447.418 | 420.17 | 447.347 | A$_2$ | 416.888 |
| | E$_1$ | 484.483 | 464.93 | 485.980 | E | 439.614 |
| | E$_2$ | 486.661 | 464.36 | 486.150 | E | 439.790 |
| 0 0 3 | B$_1$ | 764.073 | 732.43 | 763.519 | A$_1$ | 664.079 |
| | A$_2$ | 764.112 | 733.47 | 763.543 | A$_2$ | 664.202 |
| | E$_1$ | 623.966 | 586.69 | 623.904 | E | 566.925 |
| | E$_2$ | 623.909 | 587.55 | 623.963 | E | 567.015 |
| 0 0 4 | A$_1$ | 779.811 | 776.16 | 779.725 | A$_1$ | 689.459 |
| | B$_2$ | 783.640 | 783.91 | 781.847 | A$_2$ | 689.207 |
| | E$_1$ | 961.292 | 917.30 | 960.490 | E | 825.383 |
| | E$_2$ | 960.857 | 919.24 | 960.579 | E | 825.524 |
| 0 1 0 | B$_1$ | 1,013.573 | 1,018.95 | 1,017.495 | A$_1$ | 935.768 |
| | A$_2$ | 1,036.858 | 1,038.29 | 1,027.452 | A$_2$ | 945.547 |
| | E$_1$ | 1,018.895 | 1,008.94 | 1,023.138 | E | 933.720 |
| | E$_2$ | 1,009.382 | 1,010.33 | 1,013.343 | E | 938.159 |
| 0 1 1 | B$_1$ | 1,164.413 | 1,169.282 | 1,157.813 | A$_1$ | 1,091.240 |
| | A$_2$ | 1,178.154 | 1,182.743 | 1,171.147 | A$_2$ | 1,102.316 |
| | E$_1$ | 1,183.966 | 1,182.979 | 1,181.927 | E | 1,122.545 |
| | E$_2$ | 1,183.676 | 1,183.288 | 1,182.336 | E | 1,131.506 |
| 0 1 2 | A$_1$ | 1,383.962 | 1,389.035 | 1,372.966 | A$_1$ | 1,255.006 |
| | B$_2$ | 1,423.217 | 1,427.359 | 1,414.927 | A$_2$ | 1,271.686 |
| | E$_1$ | 1,408.533 | 1,414.258 | 1,398.004 | E | 1,267.221 |
| | E$_2$ | 1,443.195 | 1,448.522 | 1,431.945 | E | 1,280.415 |
| 0 2 0 | A$_1$ | 1,648.554 | 1,628.67 | 1,636.359 | A$_1$ | 1,407.586 |
| | B$_2$ | 1,659.193 | 1,651.28 | 1,648.221 | A$_2$ | 1,436.635 |
| | E$_1$ | 1,637.115 | 1,629.309 | 1,679.237 | E | 1,404.920 |
| | E$_2$ | 1,656.584 | 1,646.858 | 1,662.888 | E | 1,418.014 |
| 0 0 0 | A$_1$ | 1,382.996 | 561.00 | 1,381.794 | A$_1$ | 1,191.310 |
| | B$_2$ | 1,382.996 | 561.00 | 1,381.794 | B$_2$ | 1,191.310 |

ZPVE
the symmetry eigenvectors. The convergence of the low energy levels requires long basis sets leading to Hamiltonian matrices of 18,755 x18,755 elements. In the case of the G12 species, the matrices factorize by symmetry into eight blocks which dimensions are 1815 (A1, B2), 1,518 (B1), 1,507 (A2), and 3,025 (E1, E2). For the G6 species, the corresponding submatrix dimensions were 3,333 (A1), 3,322 (A2), and 6,050 (E), whereas for the G4 species, the dimensions were 4,840 (A1, B2), 4,543 (B1), and 4,532 (A2).

The resulting energy levels are shown in Table 6 and they are classified using symmetry and the \( \nu_7, \nu_9 \) and \( \nu_{15} \) quantum numbers. For the main isotopologue, the energies are compared with those of Kreglewski (1989) obtained from experimental parameters. The computed levels denote a slight improvement with respect to the work of Senent (2018), after using longer expansions for the kinetic energy parameters. The aim was to increase precision considering that isotopic shifts are relatively small. We observed that the vibrational energies are very sensitive to the kinetic contributions. It can be pointed out that their computations in the deuterated forms is not straightforward.

Each energy level splits into six components corresponding to the six minima of the potential energy surface. Their distributions are represented in Figure 4. In the G12 species, the levels split into two non-degenerate and two double-degenerated sublevels. The components of the ground vibrational state were computed to lie at 0.000 (A1), 0.163 (B2), 0.325 (E1), and 0.407 (E2) cm\(^{-1}\). Very small shifts are found for \( ^{13}\text{CH}_3\text{-NH}_2 \), whereas for \( ^{15}\text{CH}_3\text{-NH}_2 \), the subcomponents are close in energy (0.000 (A1), 0.153 (B2), 0.322 (E1), and 0.398 (E2)). The non-degenerate components \( B_1 \) and \( A_2 \) of the \( \nu_{15} \) fundamental (0 0 1) were obtained to lie at 265.572 and 266.117 cm\(^{-1}\) in the main isotopologue and at 264.441 and 264.995 cm\(^{-1}\) in \( ^{13}\text{CH}_3\text{-NH}_2 \), and at 264.428 and 264.936 cm\(^{-1}\) in \( ^{15}\text{CH}_3\text{-NH}_2 \). For \( \nu_9 \), the corresponding components of the (0 1 0) level were obtained to lie at 771.083 and 775.011 in the main isotopologue and at 763.413 and 769.602 cm\(^{-1}\) in \( ^{13}\text{CH}_3\text{-NH}_2 \), and at 763.413 and 769.602 cm\(^{-1}\) in \( ^{15}\text{CH}_3\text{-NH}_2 \). It may be concluded that the effects of isotopic substitutions on the heavy atoms are less relevant for the torsional excitation than for inversion excitations.

As was expected, isotopic effects on the low-lying energies are more noticeable for the deuterated species. For \( ^{3}\text{CH}_3\text{-NDH} \), the nondegenerate components of the \( \nu_6 \) and \( \nu_{15} \) fundamentals have been computed to be 236.260 and 236.470 cm\(^{-1}\), and to be 715.178 and 718.848 cm\(^{-1}\). The gaps among subcomponents of the ground vibrational state are smaller than in the hydrogenated species. The isotopic substitution in one methyl group hydrogen breaks ten the degeneracy of the CDH\(_2\)NH\(_2\) levels. The ground vibrational state splits into two \( A_1 \), two \( B_2 \), one \( B_1 \) and one \( A_2 \) components lying in the 0.000–1.672 cm\(^{-1}\) range.

**CONCLUSION**

This work describes the shifts of spectroscopic parameters and the symmetry changes due to the isotopic substitutions for various probably detectable methylamine isotopologues, \( ^{13}\text{CH}_3\text{NH}_2, ^{15}\text{CH}_3\text{NH}_2, ^{13}\text{CH}_3\text{NHD}, \) and \( ^{15}\text{CH}_3\text{NHD} \). A variational procedure and VPT2 theory are employed for describing rovibrational properties with a special attention to the far infrared region. For all the isotopologues, the levels up to 1,500 cm\(^{-1}\) over the ground vibrational state are determined variationally and classified using the G12, G6 and G4 MSG properties. For the main isotopologue, the ground vibrational state splits into six components computed to lie at 0.000 (A1), 0.163 (B2), 0.325 (E1), and 0.407 (E2) cm\(^{-1}\). Very small differences are found for \( ^{13}\text{CH}_3\text{NH}_2 \), whereas for \( ^{15}\text{CH}_3\text{NH}_2 \), the computed subcomponents are close in energy (0.000 (A1), 0.153 (B2), 0.322 (E1), and 0.398 (E2)). Isotopic shifts are relevant for the deuterated forms, whereas the effects of substitution of heavy atoms are less relevant for the torsional excitation than for inversion excitations. Small variations of the kinetic energy parameters carry out substantial displacements of the levels. It can be pointed out that their computations in the deuterated forms is not straightforward.

**DATA AVAILABILITY STATEMENT**

The original contributions presented in the study are included in the article/Supplementary Material, further inquiries can be directed to the corresponding authors.

**AUTHOR CONTRIBUTIONS**

MA has performed the new ab initio calculations. MS was responsible for the variational calculations, the assignments of the levels, and for writing the manuscript.

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