Surface effects in solar-like oscillators

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Abstract. Inaccurate modelling of the near-surface layers of solar models causes a systematic difference between modelled and observed solar mode frequencies. This difference—known as the “surface effect” or “surface term”—presumably also exists in other solar-like oscillators and must somehow be corrected to accurately relate mode frequencies to stellar model parameters. After briefly describing the various potential causes of surface effects, I will review recent progress along two different lines. First, various methods have been proposed for removing the surface effect from the mode frequencies and thereby fitting stellar models without the disproportionate influence of the inaccurate near-surface layers. Second, three-dimensional radiation hydrodynamics simulations are now being used to replace the near-surface layers of stellar models across a range of spectral types, leading to predictions of how some components of the surface effect vary between stars. Finally, I shall briefly discuss the future of the problem in terms of both modelling and observation.

1 Introduction

The era of space-based asteroseismology, driven chiefly by COROT [1] and Kepler [2], has provided observations of hundreds of cool main-sequence stars in which dozens of individual mode frequencies can be measured. To exploit this data, however, we need to correct for a systematic difference between observed and modelled mode frequencies caused by improper modelling of the near-surface layers of these stars: the so-called surface effect or surface term. Motivated by a newfound need to correct for the surface effect, significant progress has been achieved in the last few years and can be expected in the near future.

The purpose of this review is to first briefly recount our physical understanding of the surface effect (Sec. 2) and then review recent progress along two lines. First, several authors have proposed parametrizations of the surface effect (as a function of frequency) to suppress its influence when fitting stellar models to observed mode frequencies (Sec. 3). Second, a few research groups have begun replacing the near-surface layers of stellar models with average structures taken from detailed three-dimensional radiation hydrodynamic simulations (3D RHD, Sec. 4). Finally, I close with a few thoughts on how we might progress further on the problem of surface effects in the near future (Sec. 5).

I do not pretend that this review is exhaustive. Judging by the amount of material I excluded from my talk, it would be impossible to cover all the literature on the subject in 30 minutes. I apologize to anyone who feels their contribution has been omitted and seek to assure them that the cause is only brevity, not malice!

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2 The problem

2.1 Phenomenology of the surface effects

Suppose that one calibrates a solar model in the traditional sense by varying the mixing length parameter, initial helium abundance and initial metallicity to evolve a stellar model that matches the Sun’s current radius, luminosity and surface metallicity, with the mass fixed at 1 M⊙ and the age at the meteoritic age of the solar system. We take Model S [5] as an example. If we compute the linear adiabatic mode frequencies of this model and compare them with observed values [e.g. the low-degree data from the Birmingham Solar Oscillation Network, BiSON; 3, 4] we might hope that the differences between observed and modelled frequencies are randomly scattered about zero.

Instead, one gets the values plotted in Fig. 1. The white points indicate the differences between the mode frequencies predicted for Model S and those observed by BiSON. The discrepancy is much larger than the quoted uncertainties but it is also not random, and its structure tells us something about where the problem arises. First, the frequency differences do not depend on the angular degree ℓ, which suggests that the discrepancy lies well above the modes’ lower turning points. The low-degree data alone only tells us that the cause is not very deep in the Sun but the frequency differences of the higher-degree modes are also ℓ-independent. Because they have shallower lower turning points, this suggests that the problem is quite close to the Sun’s surface. Second, the frequency differences are close to zero at frequencies below about 2200 µHz. Higher-frequency modes have shallower upper turning points, which again implies that the problem is somewhere near the Sun’s surface. At 2200 µHz, the modes’ upper turning points are around 1 Mm below the surface, which implies that the effect really is confined to the near-surface layers.

The shaded region in Fig. 1 indicates the range of frequency covering about five radial orders either side of the frequency of maximum oscillation power νmax. This is the range in which modes oscillate with the greatest power and are thus most easily observed. It shows that the surface effect probably affects nearly all the observed modes in distant Sun-like stars, unlike the Sun, in which we observe low-frequency modes that appear unaffected by the surface effect. The best targets from the nominal Kepler mission have lowest mode frequencies equivalent to about 2300 µHz in the Sun, which is within the range of affected modes. For this reason, the surface effect is unavoidable: when fitting stellar models to individual mode frequencies, something must be done about the surface effect. In the case of the Sun, even the large separations of the modelled and observed frequencies differ by about 1 µHz. When applied to the standard scaling relations [6], this bias in the large separation corresponds to biases in mass and radius of about 3 and 1.5 per cent, respectively.1

1The scaling relations are in essence empirical, which suppresses this effect. But if the surface effect varies significantly between different stars, it could be important.

2.2 The physical cause

It may come as a surprise that we have a fairly good idea about what causes the surface effect: improper modelling of near-surface convection. Most stellar models use some form of mixing-length theory (MLT), in which the convection zone is presumed to contain buoyantly-unstable rising and falling parcels of material (see Fig. 2, left). These parcels rise or fall by one mixing length, typically parametrized in terms of the local pressure scale height, \( H_P = -dr/d\ln P \), after which they disperse, mixing the heat and composition of their origin into their new surroundings.

In reality, the flows are much more complicated, as is now understood from detailed 3D RHD simulations that accurately reproduce many observable features of convection at the Sun’s surface [see 7, for an excellent review of the Sun’s surface convection]. Let us start with one of the slow upflows. As it rises and the density decreases, so the flow expands horizontally and, to conserve mass, part of it must turn over and join whatever downflows exist (see Fig. 2, right). The rising plume ultimately appears as a granule at the surface, where the flows are chiefly horizontal. They then radiate heat to the vacuum of space before plummeting downward in narrow, turbulent intragranular lanes. Along the way back down, these downflows will draw material turning over from the widening upflows.

This is a very different picture from the calm rise and fall of MLT’s parcels and it leads to a number of effects that affect the mode frequencies. Following the thorough discussion by Rosenthal [8], we can broadly divide these into two types of effect. Model physics includes everything that is wrong with the background model that we perturb. This includes, but is not limited to, MLT’s incorrect temperature gradient, the incorrect atmospheric structure and the absence of turbulent pressure. Modal physics includes everything that is wrong with the calculation of the mode frequencies, which are affected by the perturbation to the turbulent pressure [e.g. 9], the modification of wave speeds when travelling with or against the flows [e.g. 10] and various effects of non-adiabaticity [e.g. 11]. All of these effects are most pronounced near the surface where convection becomes inefficient and the temperature gradient deviates furthest from the adiabatic value.

That so many physical effects contribute to the surface effect makes it a difficult problem to tackle piece by piece. In working on one component, one might think the problem is solved, only to find that another component returns you to square one. But it is not hopeless! We can learn how much each component might contribute and gradually add them up, bearing in mind that as our models improve, we might sometimes veer further from the observations before once again closing the gap.

3 Parametrizations

The surface effect in Fig. 1 appears to be a relatively simple function of mode frequency only. Thus, several groups have proposed parametric forms for this function whose
First, Kjeldsen et al. [12] proposed that the surface effect can be described as a power law with an index fixed to a solar-calibrated value (usually around 5 but slightly dependent on the precise physics of the stellar model). They also proposed that the magnitude of the power law be fit after rescaling the frequencies so that the stellar model being compared has the same mean density as the observed star. To rescale the frequencies so, they propose using the ratio of the large separations. This simple parametrization has been widely used since its publication [e.g. 15].

More recently, Ball & Gizon [13] proposed parametrizations based on surface perturbations and the asymptotic behaviour of the eigenmodes. Roughly speaking, the displacement eigenfunctions are exponentially decaying functions near the photosphere and, combining them with the variational principle for the linear, adiabatic oscillation equations [16], one finds that, for a sound speed perturbation or pressure scale height perturbation near the surface, the frequency shifts go either like $\nu^3 / I$ or $\nu^{-1} / I$, where $\nu$ is the mode frequency and $I$ the normalized mode inertia. These parametric forms, which Ball & Gizon [13] refer to as the cubic and inverse terms, respectively, were originally derived by Gough [17] in a discussion of the Sun’s frequency shifts over the magnetic activity cycle. The inverse term alone does not fit the data well so Ball & Gizon [13] proposed to combine it with the cubic term, giving what they call the combined surface correction.

Most recently, Sonoi et al. [14] proposed to describe the surface effect as a modified Lorentzian function and calibrated its parameters to frequency shifts induced by replacing the near-surface layers of stellar models with averaged data from hydrodynamics simulations (see Sec. 4, parameters can be fit when comparing stellar models to observations. Here I shall review the best known and compare them for the Sun.

Figure 2: A crude illustration of the difference between the mixing-length theory of convection (MLT, left) and the structure of near-surface convection suggested by 3D RHD simulations (right). In MLT, buoyantly-unstable parcels of material retain their composition and heat content while floating upwards (or sinking downwards) by one mixing length $l_{\text{MLT}}$ before dispersing their composition and heat into their new surroundings. In the 3D RHD simulations, slow, broad upflows expand as they rise through layers of decreasing density, ultimately reaching the surface and manifesting as granules. At the surface, material cools and sinks back down between the granules in rapid, cool downdrafts that we see as intragranular lanes.

Figure 3: Frequency differences, as a function of frequency, for the observed surface effect in the Sun (white points) and several parametrizations (see Sec. 3). The shaded region shows the frequency range over which the modes have their greatest power, as in Fig. 1. The parametrizations shown are a power-law [solid blue, 12], the cubic and combined formulae [dashed orange and dash-dotted red, 13] and a modified Lorentzian [dotted green, 14].
below). This parametrization is very new and has not yet been tested on observed data.

Fig. 3 shows the same data as Fig. 1 (BiSON against Model S), along with the above-mentioned parametrizations. The power law fit performs reasonably well in the shaded range around $v_{\text{max}}$ but overestimates the surface effect both where it begins to rise and at higher frequencies. The cubic and the combined terms fare better. Though the improvement by using the combined term (rather than just the cubic term) is significant for the Sun, this was not the case for the COROT target HD 52265 studied by Ball & Gizon [13]. Finally, the modified Lorentzian captures most of the low-frequency behaviour but underestimates the difference at high frequencies.

Though different in principle, it is worth mentioning several methods proposed by Roxburgh (and Vorontsov in earlier work) [20–22]. These are all based on representing the oscillation modes as simple oscillations with phase shifts at the inner and outer boundaries. The outer phase shift contains the undesired and presumably $\ell$-independent surface term whereas the inner phase shift is related to the structure of the stellar core. One can combine the frequencies into ratios of differences or so-called separation ratios that are nearly independent of the near-surface layers [20]. Otí Floranes et al. [23] computed kernels for these quantities and demonstrated that they are, indeed, largely insensitive to the near-surface layers and they have seen widespread use in asteroseismic modelling. From the same underlying principles, Roxburgh [21, 22] described methods to fit out a more general $\ell$-independent component of the frequency differences. These are too new to have been used widely.

These various parametrized methods have not yet been systematically compared with observations, though the community’s collective experience suggests that none generally leads to absurd results. Schmitt & Basu [24] conducted the most thorough study yet by inserting structural perturbations into stellar models across the HR diagram and then trying to fit the frequency differences using the solar-calibrated power law, the cubic and combined terms of Ball & Gizon [13] or the observed solar surface effect, rescaled by the large separation. The combined term by Ball & Gizon [13] appeared to fare best, although the scaled solar term also performed reasonably on the main sequence.

The parametrizations do not solve the problem of the surface effects but they at least allow us to exploit the reams of data already available while we work towards properly modelling the surface effects. The results should always be interpreted with the knowledge that the Sun remains the only star for which we can truly calibrate the frequency differences. Everything else depends on the confidence we place in how well our best-fitting models represent the stars under study.

4 Three-dimensional radiation hydrodynamics

I mentioned in Sec. 2 that the surface effect is chiefly caused by improper modelling of near-surface convection. So why not use better models of near-surface convection? This is the idea behind recent efforts to combine stellar models with 3D RHD simulations. Several groups have simulated near-surface convection from first principles in stars of various spectral types [e.g., 27–29]. These simulations are sufficiently realistic to reproduce most of the observed characteristics of the Sun’s near-surface convection [again, see 7, for a review] and it is assumed that they are similarly realistic for other stars.

The process of replacing a stellar model’s near-surface layers with averaged simulation data is becoming known as patching. The frequency differences are then computed between the patched model (the original stellar model) and the patched model (with the near-surface layers replaced). The idea of patching is not new. Rosenthal et al. [9] restricted their study of solar oscillations to modes with angular degree $\ell > 60$. These modes are trapped within the solar convection zone, so they could compare their averaged simulation data with envelope models computed using MLT. Their early results showed that replacing the equilibrium structure of the stellar model with the simulation data, averaged at constant geometric depth, already introduced a surface effect of similar magnitude to the observed effect, although a significant systematic effect remained. More
it remains unclear what is the appropriate form of the perturbation to the turbulent pressure. Both Sonoi et al. [14] and Ball et al. [25] assume that the turbulent pressure varies with the total pressure: Rosenthal et al. [9] dubbed this the gas gamma one approximation. Changing this assumption potentially affects the results by a factor of about two [9]. Moreover, it is unclear exactly what is the appropriate horizontal average to take from the simulation data. Sonoi et al. [14] and Ball et al. [25] both used averages over constant geometric depth but different averages give surface effects that differ by a few $\mu$Hz for the Sun (see Fig. 4).

Fig. 4 shows how the mode frequencies of a standard solar model [Model S again, 5] are changed by the modification of the near-surface equilibrium structure. The white points are the same differences shown in Figs 1 and 3. The solid blue, dotted green and dashed red curves show the differences in the model frequencies before and after patching with the G2-type MURaM simulation averaged over constant geometric depth, pressure or optical depth. The spread in the curves shows that uncertainty above the appropriate average introduces an uncertainty in the frequency shifts of about 0.5–1.0 $\mu$Hz. Finally, the orange squares show the remaining difference between the patched model (with the simulation averaged at constant geometric depth) and the BiSON observations. The overall surface effect is reduced substantially, though clearly a large effect remains and the remaining difference is still a surface effect. It is not yet clear if the remaining trend is because the averaged near-surface structure is still not quite right, because non-adiabatic effects have been neglected, or (most likely) both.

With these uncertainties in mind, both teams found that the surface effect is larger in stars that are hotter. Based on their cooler dwarfs, Ball et al. [25] also noted that the overall shape of the frequency differences as a function of frequency is similar in the G2-, K0- and K5-type models, but some qualitative change sets in between the F3- and G2-type models. Sonoi et al. [14], with their greater coverage of surface gravity, also found that the surface effect increases with increasing surface gravity. Within their limitations, the two groups’ results are mutually consistent. They have two simulations with similar parameters and the results agree well. Fig. 6 shows the frequency shifts for all the simulations by Ball et al. [25, left] and the simulations A and B of Sonoi et al. [14, right], which have similar parameters to models G2 and F3 of Ball et al. [25].

Both teams also compared the parametric fits described in Sec. 3, though Sonoi et al. [14] only compared their modified Lorentzian with a power law. Fig. 6 shows that a simple power law does not describe the differences between the patched and unpatched models very well. Ball et al. [25] found that the combined term was consistently superior, notably in their F3 model, but a scaled solar frequency correction fits reasonably well in their three cooler models. Sonoi et al. [14] provided simple fits to the best-fit parameters as a function of surface properties, though they did not consider a scaled solar correction or either of the corrections by Ball & Gizon [13].
Further exploitation of the 3D RHD simulations is underway, notably on non-adiabatic effects, but these early results already give some indication of how much of a surface effect is introduced by improving the background stellar model. It remains to be seen if the conclusions hold up as further surface effects are considered.

5 The future

To close, I briefly opine on how we might progress further on the problem of surface effects. The main theoretical path at this point is to further exploit the 3D RHD simulations. There is far more information available than simply the horizontally- and temporally-averaged profiles and this information can be used to investigate other components of the surface effect. But it should be remembered that even indirect conclusions drawn from the simulations can be useful. For example, the parametrizations of the surface effects tend to correlate with the mixing-length parameter in stellar models. There is good physical reason for this: both the surface effect and the mixing-length parameter are sensitive to the superadiabatic layer near the stellar surface. If the mixing-length parameter is constrained separately by the simulations [e.g. 37, 38] then the surface effect is also better constrained.

Progress is more difficult from the observational side. The best solar-like oscillators from the nominal Kepler mission show modes oscillating at frequencies nearly low enough that they are unaffected by the surface effect. If just a few more radial orders could be detected, these low frequencies could potentially be used to fit models without a surface term, though at the cost of discarding the many higher-frequency modes that are available. Alas, no imminent mission will provide such high-quality data for single targets, so we may have to wait until PLATO [39] for higher-quality data on single targets.

From the ground, however, there is tremendous potential from the Stellar Oscillation Network Group [see e.g. 40, these proceedings]. Because it observes in radial velocity, the background signal of granulation is weaker, which allows lower-frequency modes to be detected more easily. This could allow us to calibrate models directly to the unaffected frequencies and inspect the remaining frequencies to determine the surface effect after fitting the stellar model. One node of the network is fully operational and another partially so. The first results from the first node were reported at this meeting [40]. Adding nodes to the network probably represents our best chance of bringing tight observational constraints to bear on the problem of surface effects.

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To close, I briefly opine on how we might progress further. The best solar-like oscillators from the nominal frequencies could potentially be used to fit models with - just a few more radial orders could be detected, these low effects. If better constrained, the simulations [e.g. 37, 38] then the surface effects, both the surface effects and even indirect conclusions drawn from the simulations can be used to investigate other components. There is far more information available than simply path at this point is to further exploit the 3D RHD simulations. The main theoretical effects are considered.

The future is introduced by improving the background surface effects, but these early results from the SONG Hertzsprung telescope [40], these proceedings. Because it observes in radial velocity, the background signal of granulation is weaker, which allows lower-frequency modes to be detected more easily, the background signal of granulation is weaker, which allows lower-frequency modes to be detected more easily. The first results from the first node were reported at this meeting [40]. Adding nodes to the network probably represents our best chance of bringing many higher-frequency modes that are available. Alas, no more. The right correspond to the solar model and hottest model of Sonoi et al. [14] and can be compared to models G2 and F3 on the left, Figure 6: Frequency differences between various models before and after their near-surface layers are replaced with horizontally-

directional.

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