Supersymmetry Without Prejudice at the 7 TeV LHC

John A. Conley
Physikalisches Institut, Universität Bonn, Nussallee 12, 53113 Bonn, Germany

James S. Gainer
High Energy Physics Division, Argonne National Laboratory, Argonne, IL 60439 USA and Department of Physics and Astronomy, Northwestern University, Evanston, IL 60208 USA

JoAnne L. Hewett, My Phuong Le, Thomas G. Rizzo
SLAC National Accelerator Laboratory, 2575 Sand Hill Rd., Menlo Park, CA 94025, USA

Abstract

We investigate the model independent nature of the Supersymmetry search strategies at the 7 TeV LHC. To this end, we study the missing-transverse-energy-based searches developed by the ATLAS Collaboration that were essentially designed for mSUGRA. We simulate the signals for $\sim 71k$ models in the 19-dimensional parameter space of the pMSSM. These models have been found to satisfy existing experimental and theoretical constraints and provide insight into general features of the MSSM without reference to a particular SUSY breaking scenario or any other assumptions at the GUT scale. Using backgrounds generated by ATLAS, we find that imprecise knowledge of these estimated backgrounds is a limiting factor in the potential discovery of these models and that some channels become systematics-limited at larger luminosities. As this systematic error is varied between 20-100%, roughly half to 90% of this model sample is observable with significance $S \geq 5$ for 1 fb$^{-1}$ of integrated luminosity. We then examine the model characteristics for the cases which cannot be discovered and find several contributing factors. We find that a blanket statement that squarks and gluinos are excluded with masses below a specific value cannot be made. We next explore possible modifications to the kinematic cuts in these analyses that may improve the pMSSM model coverage. Lastly, we examine the implications of a null search at the 7 TeV LHC in terms of the degree of fine-tuning that would be present in this model set and for sparticle production at the 500 GeV and 1 TeV Linear Collider.
1 Introduction and Background

The LHC has had an initial run at 7 TeV with both the ATLAS and CMS experiments collecting $\sim 35 - 45 \text{ pb}^{-1}$ of useful data. Even with this low integrated luminosity these experiments have been able to extend searches far beyond the reach of the Tevatron for many new physics scenarios with, so far, null results [1, 2]. This clearly demonstrates the power of increasing the center of mass energy in the search for new physics at hadron colliders. Starting soon, the LHC is to begin a longer run at 7 TeV and is expected to collect of order $1 - 7 \text{ fb}^{-1}$ of data over the next 2 years. Such a data set will allow for a first exploration of the TeV mass scale, and if new strongly interacting particles exist in this kinematic regime, they should be observed.

A well-motivated, and perhaps most popular, possibility for new physics that may be discovered during this coming LHC run is Supersymmetry (SUSY) [3]. Both ATLAS [4] and CMS [5] have designed detailed searches for many of the SUSY partners of the Standard Model (SM) particles; these are mostly (but not exclusively) based on the assumption of mSUGRA/CMSSM-like soft breaking within the Minimal Supersymmetric Standard Model (MSSM) framework. This assumption greatly simplifies the exploration of the vast Supersymmetric parameter space. While these searches are designed to well cover the parameter space of these SUSY-breaking scenarios it is important to ascertain their discovery potential in a more general MSSM context. This is particularly worrisome in light of results from the Tevatron, where it has been realized [6, 7] that relatively light gluinos may have escaped undetected. The question then arises whether these specific scenarios and associated searches adequately describe the true breadth of the MSSM and its possible collider signatures, and whether the LHC searches as presently designed could fail to observe sparticle production. This has prompted several studies of more model independent search strategies as well as the development of simplified models [8].

Recently, we have addressed [9] this question by investigating the capability of the 14 TeV LHC to explore a more general MSSM model parameter space, i.e., that of the pMSSM (phenomenological MSSM) [7], to be described below, from the point of view of the ATLAS detector. In particular, we examined the performance of the planned ATLAS SUSY searches in exploring this more general MSSM scenario. This analysis provides insight into general features of the MSSM without reference to a particular SUSY breaking scenario or any other assumptions at the GUT scale. We found that the ATLAS mSUGRA-inspired searches, based on missing $E_T$, did surprisingly well at covering the kinematically accessible portions of this model space; we also found that some interesting exceptions can arise in these more general models. Given the lower-energy run of the LHC over the next 2 years it behooves us to determine how well the corresponding mSUGRA motivated searches designed by ATLAS would perform under these conditions, since this is the situation presently before us. This is the goal of the present paper. We note that recently there have been several mSUGRA-based studies evaluating the capability of the 7 TeV LHC run to probe that parameter space [10].
As is well known, soft SUSY breaking within the MSSM in all generality leads to a theory with over $\sim 100$ a priori free parameters which prohibits a detailed study of this theory. A number of theoretically possible scenarios exist which describe the breaking of Supersymmetry; maybe even multiple mechanisms are simultaneously responsible. Practically speaking, there are two ways to approach reducing this large number of a priori unknown parameters to something more manageable. One approach is to consider only specific, well-motivated SUSY breaking scenarios, such as mSUGRA or others. This leads to a drastic reduction in the number of free parameters (to only $\sim 3 - 5$) so that detailed analyses of the resulting parameter space can be easily achieved. A problem with performing such studies is that they may result in a bias as to the nature of SUSY signals when searching for collider or other SUSY signatures. An alternative approach is to be less prejudicial and to instead follow a bottom-up analysis which we have employed in a number of recent works [9, 11] and will make use of here. By imposing a set of theoretically and experimentally well-motivated constraints on the general MSSM (to be described below), without making any reference to the specific mechanism of SUSY breaking, we arrive at a theory with 19 TeV-scale parameters. This is known as the pMSSM, which is significantly more manageable than the full Supersymmetric parameter space, and yet allows for more breadth than is present in , e.g., mSUGRA. These parameters will then completely define and describe all aspects of TeV-scale SUSY phenomenology. Such an approach has the advantage of being more general than any given (or given set of) specific SUSY breaking scenario(s) and allows one to be in some sense agnostic about the SUSY mass spectrum.

To this end, we examine the $E_T^{\text{miss}}$-based SUSY searches developed by the ATLAS collaboration for the 7 TeV LHC [12]. We simulate the pMSSM signal for roughly 71k pMSSM models (hereafter ‘model’ refers to a point in the 19-dimensional pMSSM parameter space) that we generated in our previous work [7]. We employ SM backgrounds provided by the ATLAS Collaboration. In Section 2, we describe our SUSY model generation and LHC analysis procedure. It is important to note that we strictly adhere to the analyses as designed by ATLAS. While numerous, and perhaps improved, SUSY collider search techniques have been discussed in the literature [13], it is not our present purpose here to discuss or employ them. Section 3 contains our main results. We find the systematic error in determining the SM background to SUSY production is a limiting factor in the potential discovery of these models; in fact, some channels become systematics limited at larger luminosities. In this section we determine the fraction of our pMSSM model set that is discoverable at the 7 TeV LHC. We then examine the model characteristics in some detail that render some of the models undetectable. We find that the observability of models depends on the precise details of the sparticle spectrum and that a blanket statement of constraints on the mass of, say the gluino or squarks, cannot be made. In this Section, we also explore potential modifications to the kinematic cuts in these analyses that may improve model observability. In Section 4, we examine the implications of a null SUSY search during this run with respect

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1Even in such a case a full exploration of this large parameter space is at best difficult if not impossible with present computing power.
to the degree of fine-tuning present in these models, as well as the implications for sparticle production at a high energy $e^+e^-$ Linear Collider. A summary and our conclusions can be found in Section 5.

2 Analysis Procedure for Inclusive SUSY Production at the LHC

The purpose of this work is to explore how well mSUGRA-inspired inclusive SUSY searches (in particular the set proposed by the ATLAS collaboration [12]) apply to the larger and much more general pMSSM parameter space for the 7 TeV run of the LHC. This is similar in spirit to Ref. [9], which explored this question for the more powerful 14 TeV LHC. The pMSSM model sample that we study was generated in Ref. [7]; here, we briefly review the procedure employed to generate this sample. We then describe our procedure for generating the signal events, comparing to background, and determining the statistical criteria for discovery. We will show that we faithfully reproduce the ATLAS results in each analysis channel for their benchmark SUSY model.

As stated above, we study the 19-dimensional parameter space of the pMSSM. This set of parameters was arrived at [14] by imposing the following set of requirements onto the general R-Parity conserving MSSM: (i) the soft parameters are taken to be real so that there are no new CP-violating sources beyond those in the usual CKM matrix; (ii) Minimal Flavor Violation (MFV) [15] is assumed to be valid at the TeV scale; (iii) the first two generations of sfermions having the same quantum numbers are taken to be degenerate and to have negligible Yukawa couplings and (iv) the lightest neutralino is assumed to be the Lightest Supersymmetric Particle (LSP) and is a stable thermal WIMP. Most of these assumptions are applied in order to avoid issues associated with flavor physics constraints. With these conditions, the remaining 19 free soft-breaking parameters are given by the three gaugino masses, $M_i=1-3$, the ten sfermion masses $m_{\tilde{f}}$, the three $A$-terms for the third generation fermions ($A_{b,t,\tau}$), and the usual Higgs sector parameters $\mu, M_A$ and tan $\beta$.

To generate the specific pMSSM parameter points that we study below (hereafter referred to as our set of models), we performed numerical scans over the space formed by these 19 parameters. This required both a selection of the parameter range intervals as well as an assumption about the nature of the scan prior for how points are chosen within these intervals. These issues are both described in detail in our previous works [7, 9, 11] and the interested reader should refer to them directly. Here, we simply note that two scans were performed: one employing a flat prior beginning with $10^7$ points and one with a log prior employing $2 \times 10^6$ points. The main distinctions between these two scans directly relevant to our analysis here are that (a) all SUSY mass parameters were restricted to be $\leq 1$ TeV for the flat prior case, while for the log case the upper limit on mass parameters was raised to 3 TeV, and (b) the choice of the log prior generally leads to a more compressed sparticle
spectrum than does the flat prior case. Note that the restriction on the upper limit for the mass parameters ensures relatively large production cross sections at the LHC for the case of the flat prior model sample.

Once these points were generated, we demanded that they be consistent with a large number of both theoretical and experimental constraints in order to ensure that the model sets are valid to study. We mention the most important of these restrictions here:

(i) The spectrum is required to be tachyon free, color and charge breaking minima must be avoided, a bounded Higgs potential must be obtained and electroweak symmetry breaking must be consistent. (ii) We impose a number of flavor and electroweak constraints arising from \( g - 2, b \to s\gamma, B \to \tau\nu, \bar{B}_s \to \mu^+\mu^- \), meson–anti-meson mixing, the invisible width of the \( Z \) and \( \Delta \rho \). (iii) We demand that the LSP contribution to the dark matter density not exceed the upper bound determined by WMAP; note that the LSP is not required to saturate the measured relic density, leaving room for the existence of other dark matter candidates. Constraints from dark matter direct detection searches are also applied. (iv) We then include the restrictions imposed from the numerous direct searches for both the SUSY particles themselves as well as the extended SUSY Higgs sector at LEP. Here, some care was required as some of these searches needed to be re-evaluated in some detail due to particular SUSY model-dependent assumptions present in the analysis which we needed to remove. (v) Finally, the null results from a number of Tevatron searches are imposed. In addition to the Higgs searches, the most restrictive searches were found to be those hunting for stable charged particles and those looking for an excess of multijet plus MET events. We note that in the latter case, the search strategies were designed for kinematics expected in mSUGRA-like models. We thus were forced to simulate them in some detail, at the level of fast Monte Carlo, for our full model set. At the end of this analysis chain, \( \sim 68.4k \) models from the flat prior set survived this set of constraints, as well as a corresponding set of \( \sim 2.9k \) log prior models. These are the models that we will consider in our following analysis.

We now turn our attention to the analysis procedure that we followed in generating and analyzing the signal events from sparticle production at the 7 TeV LHC. Throughout our analysis, we adhere to the search strategies developed by ATLAS as closely as possible. In this reference, ATLAS considers 10 MET search channels, including selections where the minimum number of jets is 2, 3, or 4 and the number of leptons is 0, 1, or 2. In the dilepton case, opposite-sign (OSDL) and same-sign (SSDL) pairs are considered separately, with SSDL only being considered in association with 2 jets. Note that flavor tagged final states are not considered here. We consider 85 SUSY production processes that contribute to these 10 signatures.

Accurate estimates of the SM backgrounds for the various channels are crucial to the validity of this study. We obtained details of the background distributions presented in Ref. [12] directly from the ATLAS SUSY Group [18]. These backgrounds were produced

\[ \text{For full details, see Ref. [7]} \]
with state-of-the-art Monte Carlo event generators and the full ATLAS detector simulation. Employing these ATLAS computed backgrounds in our analysis allows us to concentrate on generating and analyzing signal events for each of the $\sim 71k$ parameter space points in our pMSSM model sample.

### 2.1 Generation of the Signal Events

The steps involved in the generation of the signal events are very similar to those detailed in Ref. [9]. Here we will briefly summarize the procedure and point out any differences in the present analysis. For the generation and analysis of events for a single model, the workflow is:

1. The spectrum and decay table was generated with a modified [9] version of SUSY-HIT [19].

2. The NLO cross sections for the 85 distinct SUSY production processes considered were computed using Prospino2.1 [20] and the CTEQ6.6M parton distribution functions [21] (which were also used in the event generation).

3. Using PYTHIA 6.418, events were generated, fragmented, showered, and hadronized for each of 85 SUSY production processes, with each process being weighted by its K-factor.

4. Detector effects were simulated using an ATLAS-tuned version of the fast detector simulation PGS4 [22] with the default isolation cuts removed.

5. The simulated events were then analyzed using the analysis cuts for the 10 ATLAS analyses listed above, as well as the isolation cuts described in Ref. [12].

We note that as in our previous work, a subset (about 1%) of the models suffered serious enough errors that the Pythia event generation halted. These “PYSTOP” models are excluded from our results.

### 2.2 Analysis Cuts

For the reader’s convenience, we provide here the full set of kinematic cuts for each analysis channel, summarizing the information given in Section 4 of Ref. [12]. All channels have a missing energy cut of $E_T^{\text{miss}} > 80$ GeV, and all analyses except the SSDL channel have a transverse sphericity cut of $S_T > 0.2$. Table 1 summarizes the cuts for the searches with $n = 2, 3, 4$ jets which are independent of the choice of lepton channel except for SSDL, which will be described below.
We complete the description of the kinematic cuts by specifying the additional cuts that are specific to the various lepton channels. For the case with zero leptons, events are rejected that have at least one lepton with $p_T > 20$ GeV. For the one-lepton channels, one lepton with $p_T > 20$ GeV is required, no additional leptons with $p_T > 10$ GeV are allowed, and the transverse mass $M_T$ of the selected lepton and the missing energy vector must satisfy $M_T > 100$ GeV. (The definition of $M_T$ can be found in Ref. [4].) For the OSDL channel, exactly two leptons with $p_T > 10$ GeV are required, and they must have opposite charge.

As mentioned above, the SSDL channel has distinct cuts; unlike all the other analyses, the three different jet selection options specified in Table 1 are not employed. Instead, two jets with $p_T > 80$ GeV are required. In addition, two leptons with $p_T > 20$ GeV, same charge, and invariant mass $m_{\ell\ell} > 5$ GeV must be present, and there is a veto on additional leptons with $p_T > 10$ GeV. The transverse mass of the leading lepton and the missing energy vector must satisfy $M_T > 80$ GeV.

Lastly, when performing our statistical analysis, the $M_{\text{eff}}$ cut is optimized for each channel, and for each pMSSM model, in steps of 400 GeV [12].

## 2.3 Statistical Procedure

To compute the significance of the signal for each search channel, we follow the statistical procedure described in detail in Refs. [9, 4], which is that employed by the ATLAS collaboration. The probability that the expected background fluctuates to the number of observed events is computed assuming that the systematic error on the background is Gaussian and the statistical error is Poissonian. A significance of $S \geq 5$ is required for the observation of a signal. As mentioned above, the $M_{\text{eff}}$ cut is optimized for each channel, and for each pMSSM model, in steps of 400 GeV [12]. As was discussed in Ref. [9], and will be further demonstrated here, the accuracy of the background estimation has a profound impact on the signal significance and the resulting search reach. In order to quantify this, we will present results assuming a 20, 50, and 100% systematic error on the background. We will also consider integrated luminosities of 0.1, 1, and 10 fb$^{-1}$.
2.4 Comparison with ATLAS Benchmark Models

The ATLAS SUSY group has published signal rates for a single mSUGRA benchmark point (SU4) in their study of Supersymmetry at the 7 TeV LHC \cite{12}. It is imperative for us to check the results of our analysis against these published results for this benchmark model before proceeding to apply our analysis to the pMSSM model set.

Here it is important to remind the reader that our SUSY signal generation, as described in detail in Ref. \cite{9}, differs slightly from the procedure employed by ATLAS. In particular, the numerical programs used to compute the SUSY spectrum and decay tables, as well as event generation, are different. Furthermore, we use, by necessity, a fast detector simulation as opposed to the ATLAS full GEANT-based simulation. Therefore, a small degree of discrepancy can be expected. The comparisons shown in Figures \ref{fig1} \ref{fig5} however, indicate that we are indeed able to faithfully reproduce the results obtained by ATLAS for this benchmark model for all of the various inclusive analyses.

Figure 1: The $M_{\text{eff}}$ distribution for the 4 jet, 0(1) lepton analysis on the left(right) for the SU4 benchmark model. The green data points represent our analysis, while the blue line is the result from the ATLAS study \cite{12}. The red shaded area represents the SM background.
Figure 2: The same as Figure 1 except for the 3 jet, 0(1) lepton analysis on the left(right).

Figure 3: The same as Figure 1 except for the 2 jet, 0(1) lepton analysis on the left(right).

Figure 4: The same as Figure 1 except for the 4(3) jet, OSDL lepton analysis on the left(right).
Figure 5: The same as Figure 1, except for the 2 jet, OSDL(SSDL) analysis on the left(right).
3 Results of the 7 TeV Analysis

In this Section, we relate the results of our study on the effectiveness of the ATLAS 7 TeV $E_T^{\text{miss}}$ analyses in detecting our pMSSM model sample. We first discuss the impact of the size of the background systematic errors on SUSY searches, and then turn to the discovery coverage of the pMSSM. We examine the characteristics which cause some models to be undetectable as well as study the effects of modifying the ATLAS SUSY analysis cuts. We remind the reader that our sample of $\sim 70k$ models is not intended to be a full description of the 19-dimensional pMSSM parameter space. However, the sample does contain numerous models which exhibit properties that are quite different than those expected in mSUGRA and thus provides insight into general features of the full MSSM.

3.1 Influence of Background Systematic Errors

As mentioned above, the size of the SM background systematic errors plays an important role in the ability of the ATLAS $E_T^{\text{miss}}$ searches to discover Supersymmetry, including the pMSSM. This is not surprising as the number of signal events necessary to reach $S = 5$ critically depends upon both the size of the estimated background itself as well as the background uncertainty. For a fixed systematic uncertainty, search channels with large backgrounds clearly require a large number of signal events in order to claim a discovery. To get a feel for this in the case of the ATLAS $E_T^{\text{miss}}$ analyses studied here, we determine the necessary number of signal events to reach the $S = 5$ level in each analysis as function of the fractional background uncertainty. We remind the reader that the SM backgrounds for each channel were supplied to us by the ATLAS SUSY working group [18]. In performing these calculations we exactly follow the discussion as given by ATLAS in Ref. [4]. Our results are displayed in Figs. 6 and 7 for the ten ATLAS $E_T^{\text{miss}}$ channels assuming 1 fb$^{-1}$ of integrated luminosity. Here, we see the number of signal events that are required to obtain the discovery criterion of $S = 5$ for various values of the final $M_{\text{eff}}$ cut. In the case of the nj0l channel, which has the largest SM background, we note that the required number of signal events is particularly large and is quite sensitive to the value of the $M_{\text{eff}}$ cut. Note that as the systematic error increases, the number of required signal events can rise drastically, in some cases by an order of magnitude or more. In particular, the difference between a reasonably low 20% systematic error and taking a 0% error (i.e., ignoring this effect) is substantial and theoretical analyses that do not include this error are thus wildly optimistic.

We will use these numerical results in our subsequent analyses of the pMSSM model coverage in these $E_T^{\text{miss}}$-based searches in the next subsection. They indicate the importance of reducing background systematic errors in order to increase the coverage of new physics parameter spaces.
Figure 6: Number of events required to reach the $S = 5$ level of discovery as a function of the fractional systematic error in the SM background for the ATLAS $E_T^{\text{miss}}$ searches for various values of the $M_{\text{eff}}$ cut. The results for the nj0l and nj1l searches are shown in the top and bottom panels, respectively. The curves are color coded from top to bottom as indicated in the legend. For higher values of the $M_{\text{eff}}$ cut, we see that the curves are essentially indistinguishable, lying on top of one another.
Figure 7: Same as the previous figure but now for the njSSDL(top) and 2jSSDL(bottom) search channels.
3.2 pMSSM Model Coverage

We now run each of our pMSSM models through the analysis chain described above. The first question we address is how well do the various search analyses cover the pMSSM model sample, or, more precisely, what fraction of these models can be discovered (or not) by these searches. Further, we also determine which of the analyses provide the best model discovery capabilities. Clearly the answers to these questions will be highly sensitive to the assumed values of both the integrated luminosity and the estimated SM background uncertainty. Figure 8 shows the fraction of the pMSSM models that can be discovered with \( S \geq 5 \) in each of the ATLAS \( E_T^{\text{miss}} \) channels for the flat prior model set as a function of the integrated luminosity assuming three different choices for the background systematic error. The corresponding results obtained in the case of the log prior model set can be found in Fig. 9. Here, we again emphasize that our pMSSM sample is not meant to provide full coverage of the 19-dimensional parameter space (such coverage would be computationally prohibited). However both the very large number of models in our pMSSM sample, and the distinct characteristics they possess, make this sample an ideal testbed for this set of mSUGRA designed search strategies. Our fractional results based on our pMSSM model set are thus indicative of the behavior of the MSSM under these search routines.

These figures reveal a number of interesting results: (i) The size of the background systematic errors makes a significant impact on model coverage for all search channels and integrated luminosities. For the searches with significant SM backgrounds, i.e., the nj0l and nj1l channels, variation in the background uncertainty leads to substantial changes in the capability to observe the model sample. The search least affected by systematics is 2jSSDL since the backgrounds in this case are quite small. This behavior confirms the results of the previous subsection. (ii) The model coverage in almost all cases is significantly better for the flat prior model set than for the log prior sample. This, too, is not very surprising since the masses of the sparticles in the log prior case extend out to much larger values and the sparticle spectrum is generally more compressed in this set [7]. The latter leads to softer jets and leptons in the corresponding cascade decays which have a more difficult time passing the analysis cuts. (iii) For all values of the background systematic error, the nj0l channels yield the best model space coverage with 4j0l affording the best discovery opportunity. In fact, we see that the channels which require more jets to be present have a better chance of being observed for the nj0l and nj1l searches. For the flat prior sample, the 4j0l analysis with low background systematics is observed to cover a very large fraction of the model set by itself once significant integrated luminosities are obtained. (iv) As the number of leptons required to be present in the final state increases, the model coverage is found to decrease significantly, especially for smaller values of the integrated luminosity. This is due to the fact that the branching fractions for leptons to appear in squark and gluino induced cascade decays are generally not very large in our model sample, as we have seen in our earlier work [9]. (v) Independently of the specific \( E_T^{\text{miss}} \) search, as the background systematic errors become large, the pMSSM model coverage is seen to increase more slowly with the integrated luminosity. Some of the search channels nearly saturate at high luminosity due
Figure 8: Fraction of flat prior pMSSM model set that can be observed with \( S \geq 5 \) in the \( n \j0 \) (top-left), \( n \j1 \) (top-right), \( n \j0 \jSDL \) (bottom-left), and \( 2 \jSSDL \) (bottom) search channels as a function of the integrated luminosity. The solid (dashed, dotted) curves in each case correspond to \( n=4(3,2) \), respectively for the \( n \j0 \), \( n \j1 \), \( n \j0 \jSDL \) channels. The red (green, blue) curves correspond to background systematic uncertainties of 20(50, 100)%, respectively.
Figure 9: Fraction of log prior pMSSM model set that can be observed with $S \geq 5$ in the nj0l(top-left), nj1l(top-right), njOSDL(bottom-left), and 2jSSDL(bottom-right) search channels as a function of the integrated luminosity. The solid(dashed, dotted) curves in each case correspond to $n=4(3,2)$, respectively for the nj0l, nj1l, njOSDL channels. The red(green, blue) curves correspond to background systematic uncertainties of 20(50, 100)$\%$, respectively.
to the large background uncertainties and thus become systematics dominated.

As discussed above, the final step in the ATLAS $E_T^{\text{miss}}$ analyses is to apply a cut on $M_{\text{eff}}$, where the particular value of $M_{\text{eff}}$ that is chosen (in units of 400 GeV) is the one that maximizes the signal significance given the SM background and its corresponding uncertainty. This choice not only depends upon the particular channel but also on the amount of integrated luminosity. It is important to note that if this cut is taken to be too large when maximizing the signal, then the analysis will be very sensitive to the detailed shape in the tails of both the signal and expected background distributions, especially with higher luminosities. This happens when there are very few events with large values of $M_{\text{eff}}$, e.g., 2 TeV. In this situation, small fluctuations in the SM background and/or SUSY signal expectations due to limited Monte Carlo statistics can lead to inconsistencies in whether a given model is observable in a specific analysis or even whether or not it would be detected overall. This effect only occurs in the case of the search analyses designed for the 7 TeV run, as the $M_{\text{eff}}$ cut applied in the planned 14 TeV ATLAS analyses was fixed at relatively low values.

Figure 10 shows the optimized value for the $M_{\text{eff}}$ cut for the nj0l analyses, as an example, for the flat prior model sample. The three things we see here are: (i) for large background systematic errors, a harder $M_{\text{eff}}$ cut is required to optimize the search, (ii) as the number of required jets in the final state decreases, the strength of the cut can be reduced. Both of these results are also found to hold for the nj1l and njOSDL searches although the $M_{\text{eff}}$ cut itself turns out to be less important as the number of required leptons in the final state increases. (iii) Given the warning about distribution tails in the discussion above, it is a welcome result to see that in the majority of cases only a moderately strong $M_{\text{eff}}$ cut is required to optimize the signal significance. Note that there are some cases where the $M_{\text{eff}}$ cut does not contribute very much to increase the significance of the SUSY signal; this happens in particular for scenarios where the background is low and the effect of systematic uncertainties is not very significant.

It is interesting to evaluate the fraction of models that can be discovered in multiple analyses. This is important to consider as, first, it is valuable to verify the discovery of new physics in more than one channel, and second, the availability of multiple discovery channels admits for the possibility of further studies that will allow for, e.g., the extraction of sparticle masses. To be specific, Tables 2, 3 and 4 show the fraction of pMSSM models which are observed in (exactly) $n$ channels assuming a SM background systematic error of 20, 50, and 100%, respectively. Note that the distribution shifts towards more models being observed in multiple channels as the integrated luminosity increases and the background systematic error decreases, as expected.

By combining our results for these $E_T^{\text{miss}}$ searches, we can also determine the fraction of pMSSM models that are undetected in all of the 7 TeV search analyses designed by ATLAS; this corresponds to the case of $n = 0$ in these Tables. Figure 11 presents the fraction of pMSSM models which are undetected in all of the search channels as a function
Figure 10: Optimized $M_{\text{eff}}$ cut for the flat prior model set for the 4j0l (top), 3j0l (bottom left) and 2j0l analyses (bottom right). The red (green, blue) histograms correspond to background systematic uncertainties of 20(50, 100)%, respectively. An integrated luminosity of 1 fb$^{-1}$ has been assumed in these figures for purposes of demonstration.
| # anl. | Flat $\mathcal{L}_{0,1}$ | Flat $\mathcal{L}_{1}$ | Flat $\mathcal{L}_{10}$ | Log $\mathcal{L}_{0,1}$ | Log $\mathcal{L}_{1}$ | Log $\mathcal{L}_{10}$ |
|-------|-----------------|-----------------|-----------------|-----------------|-----------------|-----------------|
| 0     | 38.172          | 7.550           | 0.9965          | 63.64           | 43.988          | 22.92           |
| 1     | 9.2928          | 4.1988          | 0.90862         | 5.376           | 4.8674          | 5.8482          |
| 2     | 8.7432          | 4.6665          | 1.6102          | 3.6687          | 5.6665          | 6.0298          |
| 3     | 41.836          | 59.878          | 39.573          | 26.008          | 34.907          | 35.38           |
| 4     | 0.65686         | 4.9257          | 7.9422          | 0.25427         | 2.2158          | 6.4657          |
| 5     | 0.53472         | 4.2629          | 6.7163          | 0.47221         | 2.0341          | 4.8311          |
| 6     | 0.54366         | 8.5391          | 13.494          | 0.32692         | 3.0875          | 6.5383          |
| 7     | 0.067026        | 2.5217          | 8.9044          | 0.21794         | 1.453           | 4.1773          |
| 8     | 0.062558        | 1.2288          | 5.6364          | 0.036324        | 0.72648         | 2.2884          |
| 9     | 0.077452        | 1.2958          | 6.548           | 0               | 0.58118         | 2.9422          |
| 10    | 0.013405        | 0.93241         | 7.6711          | 0               | 0.47221         | 2.579           |

Table 2: The fraction of models that are observed in (exactly) $n \, E_T^{\text{miss}}$ search channels assuming a SM background systematic error of 20%.

| # anl. | Flat $\mathcal{L}_{0,1}$ | Flat $\mathcal{L}_{1}$ | Flat $\mathcal{L}_{10}$ | Log $\mathcal{L}_{0,1}$ | Log $\mathcal{L}_{1}$ | Log $\mathcal{L}_{10}$ |
|-------|-----------------|-----------------|-----------------|-----------------|-----------------|-----------------|
| 0     | 54.756          | 21.772          | 4.8782          | 71.558          | 55.903          | 32.546          |
| 1     | 14.143          | 10.547          | 4.847           | 8.1729          | 7.3011          | 9.8801          |
| 2     | 7.8435          | 11.453          | 9.959           | 5.0854          | 7.1195          | 12.532          |
| 3     | 22.552          | 42.949          | 40.705          | 14.857          | 24.228          | 28.478          |
| 4     | 0.29938         | 4.1407          | 8.3533          | 0.18162         | 1.7436          | 4.5768          |
| 5     | 0.15788         | 3.1562          | 7.619           | 0               | 1.3803          | 3.4871          |
| 6     | 0.1415          | 3.3036          | 9.1487          | 0.072648        | 1.0534          | 3.4871          |
| 7     | 0.061068        | 1.4075          | 6.049           | 0.036324        | 0.79913         | 1.9615          |
| 8     | 0.031279        | 0.58536         | 3.6166          | 0.036324        | 0.32692         | 1.4166          |
| 9     | 0.013405        | 0.43493         | 2.9716          | 0               | 0.036324        | 1.235           |
| 10    | 0.0014895       | 0.25172         | 1.853           | 0               | 0.10897         | 0.39956         |

Table 3: Same as the previous Table but now assuming a SM background systematic error of 50%.
of integrated luminosity for both the flat and log prior sets. In the flat prior case we see that as the integrated luminosity increases, the model coverage substantially improves, and approaches (or exceeds) $\sim 95\%$ for $10 \text{ fb}^{-1}$ with SM background uncertainties of $50\%$ or less. In the log prior case, the improvement in pMSSM model coverage as the luminosity increases is much more gradual as we expected. However, even in this case, at high integrated luminosities substantial model coverage is seen to be obtainable at $7 \text{ TeV}$.

This figure also shows the important payoff between increasing the integrated luminosity and decreasing the SM background systematic error in terms of pMSSM model coverage. (Of course, increased luminosity often results in decreased systematic errors, up to a point.) For example, it is interesting to compare the effectiveness of the analyses for the flat prior set assuming $\delta B = 100\%$ and $\mathcal{L} = 5(10) \text{ fb}^{-1}$ with other values. Figure 11 shows that taking $\delta B = 50\%$ and $\mathcal{L} = 0.65(1.4) \text{ fb}^{-1}$ or $\delta B = 20\%$ with $\mathcal{L} = 0.20(0.39) \text{ fb}^{-1}$ produces essentially identical model coverage. This demonstrates that small reductions in the SM background uncertainty can be worth a significant amount of increased integrated luminosity in terms of pMSSM model coverage.

Another very important message to take home from this figure is that for the integrated luminosity collected during the 2010 LHC run at $7 \text{ TeV}$ ($\sim 35 \text{ pb}^{-1}$ for ATLAS), some significant fraction of these pMSSM models should already have been observed at the $S = 5$ level. Explicitly, for a background systematic error of $20(50,100)\%$ we find that $46(28,15)\%$ of the flat prior model set should have been discovered; in the log prior case the corresponding results are found to be $30(24,14)\%$. Since these are discovery results, an even greater portion of the pMSSM model sample would be expected to be excluded by these analyses. This shows the incredible power of going from Tevatron energies up to the $7 \text{ TeV}$ LHC in performing searches for massive objects, such as SUSY sparticles, even when only small amount of integrated luminosity is available.

Table 4: Same as the previous Table but now assuming a SM background systematic error of $100\%$.

| # anl. | Flat $\mathcal{L}_{0.1}$ | Flat $\mathcal{L}_1$ | Flat $\mathcal{L}_{10}$ | Log $\mathcal{L}_{0.1}$ | Log $\mathcal{L}_1$ | Log $\mathcal{L}_{10}$ |
|--------|--------------------------|----------------------|-------------------------|--------------------------|----------------------|-------------------------|
| 0      | 74.112                   | 47.23                | 17.635                  | 81.911                   | 69.016               | 47.875                  |
| 1      | 13.894                   | 16.834               | 15.996                  | 9.8438                   | 10.825               | 14.094                  |
| 2      | 4.4759                   | 13.331               | 21.917                  | 3.1602                   | 7.7007               | 15.91                   |
| 3      | 7.3282                   | 18.166               | 26.186                  | 4.9401                   | 10.607               | 15.365                  |
| 4      | 0.10575                  | 1.8827               | 6.478                   | 0.036324                 | 0.79913              | 2.6153                  |
| 5      | 0.037237                 | 1.0322               | 4.7174                  | 0.036324                 | 0.32692              | 1.7436                  |
| 6      | 0.023832                 | 0.7075               | 3.3008                  | 0                        | 0.32692              | 1.0171                  |
| 7      | 0.019363                 | 0.57345              | 2.1703                  | 0.072648                 | 0.36324              | 0.87178                 |
| 8      | 0.0029789                | 0.16831              | 1.0025                  | 0                        | 0.036324             | 0.36324                 |
| 9      | 0.0014895                | 0.064047             | 0.46474                 | 0                        | 0                    | 0.10897                 |
| 10     | 0                        | 0.011916             | 0.13257                 | 0                        | 0                    | 0.036324               |
Figure 11: Fraction of flat prior(top) or log prior(bottom) pMSSM model sets which are undetected after combining all of the ATLAS $E_T^{\text{miss}}$ search analyses. The red(green, blue) curves correspond to background systematic uncertainties of 20(50, 100)%, respectively.
3.3 Why are Models not Detected by the ATLAS $E_T^{\text{miss}}$ Searches?

Here, we investigate the main reasons why some pMSSM models are not discoverable in the ATLAS $E_T^{\text{miss}}$ searches at 7 TeV. We addressed this question in some detail in our earlier work for the case of the analyses designed for the 14 TeV LHC [9], so our discussion here will not be as extensive. Clearly, many of our previous results will carry over qualitatively into the present 7 TeV analysis.

There are multiple explanations as to why some pMSSM models are undetected by the $E_T^{\text{miss}}$ searches, the most obvious one being small production cross sections for the colored sparticles that initiate the familiar SUSY cascades. As an example, we note that for our pMSSM models in the flat prior set, the cross sections for the production of gluino and squark pairs are found to cover an enormous range of several orders of magnitude as can be seen in Fig. 12 (recall that the upper limit on sparticle masses in our flat model set is $\sim 1$ TeV). Here we see that the large (or small) values of the gluino pair cross section is completely uncorrelated with the corresponding values for first generation squarks within a particular model. Furthermore, by summing over all of the QCD production channels involving gluinos and/or first generation squarks (i.e., $\tilde{g}\tilde{g}$, $\tilde{g}\tilde{q}$, $\tilde{q}\tilde{q}$ and $\tilde{q}\tilde{q}^*$) we obtain an approximate handle on the total overall rate for SUSY production which we see ranges over four orders of magnitude. Note that for any particular value of the squark or gluino mass, the corresponding production cross section itself can vary by up to an order of magnitude or more depending upon the remainder of the pMSSM model spectrum.

While it is certainly clear from this figure that some models have too small a cross section to be discovered, the bottom-right panel indicates that this cannot be the entire explanation. Here we show the search significance, $S$, of the 4j0l channel (as it is the most powerful channel in terms of discovery capability) as a function of the total NLO QCD production cross section assuming $L = 1$ fb$^{-1}$ and $\delta B = 50\%$. Here we observe that (i) there are models with cross sections $\sim 20$ pb which are missed by this analysis, while (ii) there are models with cross sections $\sim 100$ fb which are discovered. (iii) For any given value of the cross section, the range of the significance is large and can be up to two orders of magnitude or more. This validates the claim that there are reasons other than small production cross sections that render models unobservable by these $E_T^{\text{miss}}$ analyses. (iv) For any given gluino mass there is a strong correlation of the signal significance with the mass of the LSP. Clearly when these two masses are close the average $p_T$ of the jets will be softer and this will make it more difficult to pass analysis cuts. Also if the LSP mass is large then that implies even larger squark and gluino masses that will result on average in smaller production cross sections. In the case of the nj0l analyses, a larger number of signal events is required for discovery due to the sizeable SM backgrounds and hence such models will be missed by these analyses. Visibility will then require the production of leptons with significant $p_T$ in cascade decays in order to pass the lower background nj1l, njOSDL and 2jSSSDL searches. Unfortunately, lepton branching fractions are low in these cascades in our model sample (since, e.g., sleptons are heavy) and thus some models will be missed entirely.
Figure 12: (Top left) NLO first generation squark and gluino pair production cross sections at $\sqrt{s} = 7$ TeV as a function of their masses for the flat prior model set. The green(red) points represent the gluino(squark) cross sections. (Top right) Correlation of the squark pair and gluino pair NLO cross sections in the flat prior set. Each point represents one model. (Bottom left) Total NLO QCD production cross section distribution for the flat model set. (Bottom right) Search significance of the 4j0l analysis as a function of the total NLO QCD production cross section assuming $L = 1$ fb$^{-1}$ and $\delta B = 50\%$. The solid line highlights the $S = 5$ discovery level and the color code reflects the mass of the LSP.
Of course, models that are lepton-rich will automatically fail all the nj0l analyses since they veto events with high $p_T$ leptons, but will be picked up by the searches containing leptons.

Though the production cross section for SUSY particles is reasonably well correlated with their masses, we can ask more directly if larger sparticle masses lead to their non-observation in these searches. Figure 13 shows that, indeed, models with lighter squarks or gluinos tend to lead to signals with greater significance in the 4j0l channel. However, as we can also see from this Figure, this is not true universally, e.g., there are many models with gluino (lightest squark) masses below 300 (200) GeV that have $S < 5$, while conversely there are models with 1 TeV gluinos that have $S > 5$. We see that for any given squark or gluino mass the value of $S$ can vary significantly. The top panel of Fig. 14 displays this property even more strongly where we see that these results hold even when all of the $E_T^{miss}$ searches are combined. This Figure shows the set of flat prior models that are unobservable in all the search channels in average light squark mass–gluino mass plane. Note that there are a significant number of these models which contain light squarks and gluinos. Thus while the masses of the colored sparticles do play an important role in model observability clearly there are additional important factors.

In the lower panels of Fig. 14 we see that the mass splitting between squarks and/or gluinos and the LSP can play an important role in determining model observability as was first noted in Ref. [6] and was seen explicitly in our earlier work on the generation of the pMSSM models [7] and the 14 TeV ATLAS SUSY analyses [9]. The obvious reasoning here is that as the degeneracy in the spectrum increases and mass splittings become smaller, the values of, e.g., the $p_T$ of the jets, will be reduced so that it will be more difficult to satisfy any of the analysis cuts. These figures show this result explicitly. Note, however, that, e.g., in the case of light gluinos with small gluino-LSP splittings there are many models which are still
discoverable in the 4j0l channel. The reason for this is that while the efficiency for passing the 4j0l analysis cuts may be quite low for small mass splittings, as seen in Fig. 15, the cross section to produce the lighter gluinos/squarks is very large and more than compensates for these low efficiencies, especially if there are any additional hard jets in the event from ISR. However, there are numerous unobservable models that have larger raw sparticle production cross sections than observable models with somewhat similar spectra; the difference then being in their respective abilities to pass the necessary analysis cuts.

Another cause for models being undetected is the occurrence of detector-stable sparticles at the end of gluino or squark induced decay chains instead of the LSP [9]. This happens with reasonable frequency in both the 7 and 14 TeV analyses. In such cases, the amount of $E_T^{\text{miss}}$ that is produced is substantially decreased which reduces the capability of the relevant models to pass any $E_T^{\text{miss}}$ analysis requirements. Most commonly, these sparticles are actually long-lived charginos that are reasonably degenerate with the LSP in wino- or Higgsino-like LSP scenarios. In these cases, searches for long-lived sparticles, as discussed below, will be an important supplement to the conventional $E_T^{\text{miss}}$ searches. Of course, a loss of the $E_T^{\text{miss}}$ signature can happen in other ways. For example, if the initial squark or gluino produces a very long decay chain then the particles produced at the end of such a chain will be somewhat soft. In some cases this may lead to the inability to pass the necessary $p_T$ and/or $E_T^{\text{miss}}$ requirements for the various $E_T^{\text{miss}}$-based searches and the model will not be observed. Such long decay chains were shown to occur with a reasonable frequency in our earlier work [9] and can be a contributor to models failing to pass the analyses requirements.

There are, of course, other reasons that prevent models from being discovered. As noted above, subtleties in any sector of the sparticle spectrum can make a significant difference as to whether a given model is observed by various analyses. Here, we will discuss a couple of examples where this occurs. As in Ref. [9], the approach we follow is to compare a model which fails to be observed in all search channels to one with a similar spectrum (dubbed a ‘sister’ model) that is detected in at least one channel and then examine the difference between them. For this study, we concentrate on the more difficult cases by taking the flat prior model sample and assume $\mathcal{L} = 10 \text{ fb}^{-1}$ and $\delta B = 20\%$; this leaves only $\sim 670$ models that are not observed. In order to avoid the statistical issues associated with the tails of the $M_{\text{eff}}$ distribution discussed above, and to further reduce this model set to a more manageable size, we will only consider models whose optimized $M_{\text{eff}}$ value is $\leq 800 \text{ GeV}$. We note that a large fraction of models in this set have relatively heavy LSPs with masses in excess of 400 GeV. We now discuss two brief examples of these comparisons.

Figure 16 shows a comparison of two similar models, 8944 (observed in the 3,4jOSDL channels) and 21089 (missed by all analyses), that have comparable total colored sparticle production rates (3.4 and 4.6 pb, respectively). Both of these models are not observed in the nj0l searches since the lighter squarks are too close in mass to the LSP to produce hard jets. The gaugino sectors of these two models are quite similar (with the LSP and $\tilde{\chi}_2^0$ being

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3Here, efficiency is defined as the fraction of generated signal events that pass the analysis cuts.
Figure 14: (Top) Flat prior models that are unobservable in all of the $E_T^{\text{miss}}$-based search analyses in the average light squark -gluino mass plane. (Bottom) Flat prior models that pass(green) or fail(red) the 4j0l analysis in the gluino(lightest squark) mass vs gluino-LSP(lightest squark-LSP) mass splitting plane in the left(right) panel. $\mathcal{L} = 1 \text{ fb}^{-1}$ and $\delta B = 50\%$ have again been assumed.
Figure 15: The efficiency for passing the 4j0l analysis cuts as a function of the (green)gluino- or (red)squark-LSP mass splitting. Here, efficiency is defined as the fraction of generated signal events that pass the analysis cuts.
Figure 16: The top panels compare the leading jet (left) and leading lepton (right) $p_T$ spectra for models 8944 and 21089. The bottom panels show the sparticle spectra for these two models.
Higgsino-like and $\tilde{\chi}_3^0$ being bino-like), while their colored sparticle spectra are somewhat different. In either model the decay of $\tilde{\chi}_3^0$ allows for the OSDL production through an intermediate slepton which has sufficient $p_T$ to pass the analysis requirements. However, while 8944 has a $\tilde{u}_R$ with mass below that of the gluino (which is light enough to give a reasonable cross section), allowing for the decay into $\tilde{\chi}_3^0$, only $\tilde{d}_R$ is (sufficiently) heavier than the $\tilde{\chi}_3^0$ in model 21089. In this case, $\tilde{d}_R$ is also much more massive than the gluino, through which it will dominantly decay, and so it will not have a large enough branching fraction into $\tilde{\chi}_3^0$ to produce the OSDL signature.

Figure 17 compares models 9781 (discovered in the 2jSSDL channel) and 20875 (completely missed) that have total colored sparticle production cross sections of 1.3 and 1.1 pb, respectively, but yet produce too few hard jet plus $E_T^{miss}$ events to be found in the nj0l channels due to spectrum compression. Model 9781 is quite interesting as the charginos and lightest three neutralinos are highly mixed combinations of winos and Higgsinos. In this
model, $\tilde{u}_R$ (which is relatively light) decays to $j + \tilde{\chi}_2^0$ with a $\sim 98\%$ branching fraction. Since $\tilde{\chi}_2^0$ has a large bino content, it decays $\sim 95\%$ of the time through sleptons which subsequently decay directly to the LSP with a branching fraction of $\sim 45\%$. Thus model 9781 can easily populate the leptonic final state and since the neutralinos are Majorana fermions, the 2jSSDL final state becomes accessible, a channel with an extremely small background. On the other hand, model 20875 does not allow for the generation of a typical leptonic signal. This is because the $\tilde{e}, \tilde{\mu}$ are quite heavy so that the neutralinos only allow for decay to $\tau$ leptons via an intermediate on-shell $\tilde{\tau}$. This is correlated with the relative lightness of the $\tilde{\tau}$ as well as the Higgsino-like LSP. In addition, the lightest squarks decay primarily directly to the LSP which will not produce any high-$p_T$ leptons.

These two examples demonstrate that the full sparticle spectrum may conspire to render a model undiscoverable in the $E_T^{\text{miss}}$-based analysis suite, even if the colored sparticle cross section is large. Discovery is not based on the value of the squark and/or gluino masses alone and blanket limits that claim $m_{\tilde{q}, \tilde{g}}$ are ruled out below some value cannot be set.

### 3.4 Detector Stable Sparticles in Cascades

As we mentioned above, one of the reasons that some pMSSM models may not be observed in the ATLAS $E_T^{\text{miss}}$ analyses is that squark and gluino cascade decays can sometimes lead to a final state with low $E_T^{\text{miss}}$. In many cases this is due to the existence of long-lived sparticles, usually charginos, which appear with sizable branching fractions in such cascade chains and are essentially detector stable. Particles that decay outside the detector when produced at the LHC would provide a dramatic signal of new physics (see [23] and references therein). In fact, data from the LHC are already extending the mass limits on such detector-stable sparticles [24]. Since the inclusive $E_T^{\text{miss}}$ analyses discussed above do not consider such sparticles, we will briefly sketch the 7 TeV discovery prospects for detector-stable sparticles in our model sets. As discussed in our earlier work [9], the existence of such long-lived states is relatively common in our pMSSM model sample as can be seen in Fig 18.

Our estimation of the 7 TeV LHC mass reach for each long-lived sparticle is shown in Table 5 for the specified integrated luminosities, assuming direct pair production. These results are deduced from Figure 1 of [25] by taking the geometric mean of the search reach for a 5 and 10 TeV LHC at the specified luminosities and are interpolated to the luminosities considered here where necessary. These results are somewhat conservative as only detector-stable sparticle production in the hard process is considered; additional detector-stable sparticles could be produced through cascade decays as discussed below.

The number of detector-stable sparticles of various species in our model sample is

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4Recall that we will define a particle to be detector-stable if its unboosted decay length is in at least 20m. Note that typical values of $\gamma/\beta$ for long-lived particles resulting from cascade decays are in the 2-3 range. Further note that the dependence of the number of detector-stable sparticles of various species in this model set on the value of the decay width $\Gamma_{\text{stable}}$ that is assumed is discussed in detail in [9].
Table 5: Approximate 7 TeV LHC search reaches for detector-stable sparticles of the given species with 100 pb$^{-1}$, 1 fb$^{-1}$, and 10 fb$^{-1}$ [25].

| Sparticle            | LHC Reach 100 pb$^{-1}$ GeV | LHC Reach 1 fb$^{-1}$ | LHC Reach 10 fb$^{-1}$ |
|----------------------|------------------------------|-----------------------|------------------------|
| $\tilde{\chi}^+$ (Wino-like) | 206 GeV                     | 264 GeV               | 334 GeV               |
| $\tilde{\chi}^+$ (Higgsino-like) | 153 GeV                     | 204 GeV               | 267 GeV               |
| $\tilde{\tau}$       | 79 GeV                      | 109 GeV               | 146 GeV               |
| $\tilde{t}$           | 294 GeV                     | 363 GeV               | 441 GeV               |
| $\tilde{g}$           | 563 GeV                     | 654 GeV               | 751 GeV               |

Table 6: The second column from the left gives the number of detector-stable sparticles of various types in our model set. The next two columns show the number of such sparticles that will not be discovered after 100 pb$^{-1}$, 1 fb$^{-1}$, and 10 fb$^{-1}$ at the 7 TeV LHC, following [25].

| Sparticle | In Model Set | LHC Reach 100 pb$^{-1}$ | LHC Reach 1 fb$^{-1}$ | LHC Reach 10 fb$^{-1}$ |
|-----------|--------------|------------------------|-----------------------|------------------------|
| $\tilde{\chi}_1^+$ | 8642         | 8623                   | 3471                  | 1024                   |
| $\tilde{\tau}_1$   | 179          | 179                    | 174                   | 129                    |
| $\tilde{t}_1$       | 66           | 20                     | 9                     | 1                      |
| $\tilde{c}_R$       | 49           | 10                     | 4                     | 1                      |
| $\tilde{b}_R$       | 17           | 17                     | 17                    | 11                     |
| $\tilde{b}_1$       | 11           | 0                      | 0                     | 0                      |
| $\tilde{c}_L$       | 8            | 0                      | 0                     | 0                      |
| $\tilde{s}_R$       | 8            | 3                      | 0                     | 0                      |
| $\tilde{g}$         | 5            | 0                      | 0                     | 0                      |

This Table also shows the number of detector-stable sparticles which will not be discovered at LHC with 100 pb$^{-1}$ and 1 fb$^{-1}$ of integrated luminosity, using the approximate mass reaches presented in Table 5. We assume here that the mass reach is roughly generation-independent and that it is the same for, e.g., stops and sbottoms. This assumption is reasonable except where there could be significant $t$-channel production for the first or (to a lesser extent) second generation, for instance in the case of up or down squarks.

We now focus on the specific case of long-lived charginos, which are by far the most common long-lived sparticles in our model sets. If the production cross section for colored sparticles (times relevant branching fractions into charginos) are sufficiently large, these stable charginos should be found in searches for (effectively) stable charged particles occurring at the end of a cascade decay chain. In Fig. 18 we display the estimated value for $\sigma B$ for the production of detector-stable charginos in cascade decays in our flat prior set. (Note that this does not include the direct contribution arising from direct chargino pair production.) Here, we see that roughly $\sim 84\%$ of models with detector-stable charginos lead to $\sigma B$ values
in excess of 10 fb at 7 TeV and so we expect them to be observable in the upcoming run of the LHC. In this estimation, we assumed the largest contribution to the production cross section arises from the production of gluino and light squark species. Using the decay tables generated for each model with detector-stable charginos, we calculated the branching fraction for the gluino and light squarks to produce a stable chargino at the end of each possible decay chain and then weighted them by their corresponding production cross-sections. Note that mass information for neither the mother particles or the daughter chargino is used to indicate how likely it is that the chargino will pass the trigger criteria for detection. As we used PYTHIA to compute the LO cross-section for the light squarks, we do not separately generate the production for the various light squark species. Thus in order to obtain our estimate, we make the assumption that the overall cross section is 100% dominated by that arising from the lightest squark. This assumption will break down when the squarks are nearly degenerate, especially when their branching fractions to charginos are vastly different due to the complexities in the gaugino sector. Many of our models have a large production cross-section for colored sparticles, but the relevant branching fractions to charginos can be simultaneously quite small. This can result in very small overall production rates for stable charginos well below \( \sim 10 \text{ fb} \).

3.5 SUSY Mass Scale From \( M_{\text{eff}} \)

In our earlier work on the 14 TeV ATLAS \( E_T^{\text{miss}} \) analyses, we demonstrated that the relationship between \( M_{\text{eff}} \) and the mass of the lightest colored sparticle found in mSUGRA, i.e., \( M_{\text{eff}} \simeq 1.5 m_{\text{LCP}} \) (where LCP stands for Lightest Colored Particle), proposed long ago \[26\] does not necessarily hold in the pMSSM. This possible relationship is important as it might be used to get the first handle on the overall mass scale of the sparticle spectrum. Here, we briefly note that this result remains valid for the 7 TeV ATLAS \( E_T^{\text{miss}} \) analyses as can be seen in Fig. 19. For both the 4j0l and 2j0l channels we see explicitly that the values of \( M_{\text{eff}} \) lie mostly above the expected value of 1.5\( m_{\text{LCP}} \), especially in the low sparticle mass region. However, for lightest colored sparticle masses in excess of \( \simeq 550 - 600 \text{ GeV} \) we see that, indeed, the relationship \( M_{\text{eff}} \simeq 1.5 m_{\text{LCP}} \) provides a fairly good estimate in both of these \( E_T^{\text{miss}} \) searches.

3.6 Modifying ATLAS SUSY Analysis Cuts

Given the properties of the various sparticles in our model sets, we can try to determine whether the canonical cuts employed in the ATLAS \( E_T^{\text{miss}} \)-based search analyses can be strengthened to reduce SM backgrounds without any significant loss in the coverage of our pMSSM model space. This is certainly a non-trivial issue and the structure of our analysis, being based on the fixed ATLAS \( E_T^{\text{miss}} \) analyses cuts, is not directly set up to obtain completely definitive answers. However, it is possible to make some reasonable estimates based
Figure 18: (Top) Number of models from both the log and flat prior sets combined having a charged sparticle with an unboosted decay length above a given value. (Bottom) Distribution of the estimated cross section times branching fraction for the production of detector-stable charginos in cascade decays in the flat prior model set.
Figure 19: Correlation between the value of $M_{\text{eff}}$ and the mass of the lightest colored sparticle for the 7 TeV 4j0l(left) and 2j0l(right) ATLAS $E_T^{\text{miss}}$ channels. The red(green) points correspond to flat prior models which are missed(found) in these two search analyses.

on the information that we do have available. We will concentrate on the three nj0l analyses as they generally provide the greatest pMSSM model coverage and have large statistics. The most important kinematic quantities for these searches are the requirements on the leading jet $p_T$ and the required amount of $E_T^{\text{miss}}$. Here, we make use of the average values of the distributions in these quantities for our pMSSM model sample, as well as the corresponding fitted width of the part of the distribution below this average value for pre-selected events. This information then provides us with an estimate of where these two kinematic distributions ‘turn on,’ which we take to be the average value minus this width, on the low energy/momentum side below their peak average values.

First consider the cut on the leading jet, $p_{T1}$, for the 2(3,4)j0l analyses; ATLAS chooses the value for this cut to be 180(100,100) GeV, respectively. Fig. 20 shows the distribution of the ‘turn-on’ $p_T$ values for these three ATLAS analyses obtained from analyzing the flat prior model set. For the 2j0l analysis, we see that the lower edge of the ‘turn-on’ values lies somewhat below the cut value of 180 GeV from which we can conclude that this cut is already reasonably hard and cannot be increased without a loss of model coverage. However, for both the 3j0l and 4j0l analyses we instead observe that the ‘turn-on’ values lie above those of the ATLAS cuts by $\sim$ 20 GeV suggesting that that the $p_{T1}$ cut in these two channels may be raised without impacting coverage rates for the pMSSM.

Similarly, the nominal $E_T^{\text{miss}}$ cut imposed by ATLAS for the nj0l analyses is 80 GeV. However, there is an additional subsequent cut imposed by ATLAS based on the value of $M_{\text{eff}}$, i.e., $E_T^{\text{miss}} \geq f M_{\text{eff}}$ where $f = 0.30(0.25, 0.20)$ for the $n = 2(3, 4)$ analyses. Fig. 21 shows the distributions for the ‘turn-on’ values of $E_T^{\text{miss}}$ for these three channels employing the flat prior model set. Here we see that the lower edge of this distribution occurs at $\sim$ 160(130, 120) GeV for $n = 2(3, 4)$, respectively. This is suggestive that the nominal $E_T^{\text{miss}}$ cut made by ATLAS may be increased for these three analyses without losing significant
Figure 20: Approximate location of the lower edge of the leading jet $p_T$ distribution as a function of the number of preselected events employing the flat prior model set for the 2j0l (top), 3j0l (lower left) and 4j0l (lower right) ATLAS search analyses as discussed in the text. The color code reflects the number of models.
Figure 21: Same as in the previous figure but now for the $E_T^{\text{miss}}$ distribution.

pMSSM model coverage.

4 Implications of the 7 TeV Run

In this section, we explore some implications of a null search for Supersymmetry at the 7 TeV LHC. We examine the degree of fine-tuning that would be placed on our pMSSM model sample and we discuss the resulting expectations for sparticle production at a 500 GeV and 1 TeV Linear Collider.

4.1 Fine-tuning in the Undiscovered pMSSM Models

As has recently been discussed in the mSUGRA/CMSSM context [27, 28], it is apparent that if SUSY signatures are not discovered at the 7 TeV LHC as the integrated luminosity accumulates it is likely that the SUSY parameter space must become more fine-tuned, and
hence more problematic as a solution to the hierarchy problem. Since we know which models in our sample are discoverable (or not) by the ATLAS $E_T^{\text{miss}}$ search analyses, we can ask whether this same result also holds in the case of our pMSSM model sets.\footnote{Note that the amount of fine-tuning in both our model sets was examined in some detail in our earlier work \cite{7}}

Figure 22 display the results of this analysis assuming a background systematic error of 50\% for both the flat and log prior model samples. Clearly, in the flat prior case, one sees that as the integrated luminosity increases and more models can be discovered by ATLAS, those remaining yet \textit{undiscovered} tend to be more fine-tuned as expected. In other words, the fractional loss of models from the full distribution occurs more rapidly with increasing luminosity for models with smaller amounts of fine-tuning. This is not too surprising as, overall, models with less tuning tend to have lighter SUSY sparticle spectra and are thus more easily discovered at the LHC. On the other hand, the results from the log prior model set appear to be affected somewhat differently in that the overall shape of the fine-tuning distribution does not appear to change very much by removing models that should have been already been discovered by ATLAS as the luminosity increases. In this case, we see that there is not much of an increase in the amount of fine-tuning as the set of undiscovered models shrinks. This represents one of the few apparent differences between these two different model sets. This can be explained by the fact that while the log prior model set tend to have light sparticle spectra (though they extend out to larger mass values than do those for the flat prior models) and are thus less fine-tuned to begin with, these same spectra are generally compressed making these models more difficult to discover at the LHC as was discussed above. This would imply that the models missed by the ATLAS $E_T^{\text{miss}}$ analyses in the log prior case are generally \textit{not} much more fine-tuned than those appearing in the originally generated model set. Thus we find that the amount of fine-tuning that remains in the LHC-undiscovered pMSSM model sample can depend upon the prior used to generate the original model set.
Figure 22: Two projections of the fine-tuning distributions for models in our flat (top panels) and log (bottom panels) prior sets. The top red histogram in all panels shows the result for the full model set while the subsequently lower histograms correspond to models not observed by the ATLAS $E_T^{\text{miss}}$ search analyses for various values of the integrated luminosity as indicated, assuming a background uncertainty of 50%.
4.2 Implications of pMSSM Searches for the Linear Collider

If there are no clear SUSY signals as the 7 TeV LHC integrates more luminosity, the question arises whether the production (and study) of charged sparticles remains viable at the proposed 500 GeV Linear Collider (LC). Based on mSUGRA/CMSSM model coverage projections from both the ATLAS [12] and CMS [29] Collaborations at 7 TeV with a 1 fb$^{-1}$ integrated luminosity (as well as their results from the 2010 SUSY searches), it would seem very unlikely that either light sleptons or gauginos (other than perhaps the LSP itself) will remain kinematically accessible at a 500 GeV LC if nothing is observed. Here, we address the question whether this expectation also remains true for our pMSSM model sets. To this end we examine the set of flat and log prior models which are not detected by any of the ATLAS $E_T^{miss}$ search analyses for assumed values of both the integrated luminosity and background systematic error and then determine the part of the sparticle spectrum within these models which is kinematically accessible at a 500 GeV LC. A similar analysis can also be performed for a 1 TeV LC. We remind the reader that, e.g., in the flat prior case we have no sparticles heavier than $\sim$1 TeV.

We present the results of this analysis in various ways. Tables 7 and 8 show the number of sparticles of various species that are kinematically accessible at a 500 GeV or 1 TeV LC within the subset of ATLAS-undetected models assuming $\mathcal{L} = 1(10)$ fb$^{-1}$ with $\delta B = 50(20)$%, respectively. These two cases represent both a possibly conservative and a more optimistic performance for the LHC over the 2011-12 running period. Here we see several things: (i) In addition to the gauginos and sleptons, sparticles such as stops, sbottoms and other squarks are potentially almost as likely to also be kinematically accessible at the LC [32]. (ii) The number of models with kinematically accessible sparticles and their variety is significantly greater in the log prior sample as these models are more likely to have a lighter and more compressed sparticle spectrum (iii) The difference between the two cases presented in these Tables is quite significant; in particular, we see that for the flat prior model set there is a huge depletion in the number of unobserved models at higher luminosity and with lower background systematics. There are extremely few flat prior models remaining at high luminosity with any accessible sparticles at a 500 GeV LC. (iv) Going from a 500 GeV to a 1 TeV LC substantially increases the number of models with kinematically accessible sparticles, especially in the flat prior case. It is clear that, at least for the flat prior model sample with luminosities in excess of 1 fb$^{-1}$ at the LHC, that the 500 GeV LC does not seem to be a good place to study our pMSSM models if no signal for SUSY is found at the LHC in 2011-12.

In order to study these LC results in more detail we examine their dependence on the LHC integrated luminosity; this is shown for the 500 GeV LC in Fig. 23 and for the 1 TeV LC in Fig. 24. Here we display the fraction of the unobserved set of models that have a kinematically accessible sparticle of a particular variety. At a 500 GeV LC, this fraction

\footnote{Note that we have not performed any analysis here to ascertain whether or not a given kinematically accessible sparticle is actually observable at such a LC. See, however, the work in Refs. [30] [31].}
| Sparticle | $\sqrt{s} = 500$ GeV | $\sqrt{s} = 1$ TeV |
|-----------|------------------|------------------|
| $\tilde{e}_L$ | 107 | 3052 |
| $\tilde{e}_R$ | 260 | 3938 |
| $\tilde{\tau}_1$ | 730 | 7431 |
| $\tilde{\tau}_2$ | 30 | 1288 |
| $\tilde{\nu}_e$ | 151 | 3168 |
| $\tilde{\nu}_\tau$ | 386 | 4366 |
| $\tilde{\chi}_1^0$ | 5487 | 14,510 |
| $\tilde{\chi}_2^0$ | 2738 | 10,714 |
| $\tilde{\chi}_3^0$ | 429 | 5667 |
| $\tilde{\chi}_4^0$ | 10 | 1267 |
| $\tilde{\chi}_1^\pm$ | 4856 | 13,561 |
| $\tilde{\chi}_2^\pm$ | 94 | 3412 |
| $\tilde{g}$ | 0 | 1088 |
| $\tilde{d}_L$ | 35 | 2459 |
| $\tilde{d}_R$ | 220 | 3630 |
| $\tilde{u}_L$ | 52 | 2545 |
| $\tilde{u}_R$ | 124 | 3581 |
| $\tilde{b}_1$ | 289 | 5553 |
| $\tilde{b}_2$ | 1 | 409 |
| $\tilde{t}_1$ | 93 | 3727 |
| $\tilde{t}_2$ | 0 | 2 |

Table 7: Number of kinematically accessible sparticles from our set of 14623(1546) flat(log) prior pMSSM models that are unobservable by the ATLAS $E_T^{miss}$ searches assuming $\mathcal{L} = 1$ fb$^{-1}$ with $\delta B = 50\%$ for both a 500 GeV and 1 TeV LC.
| Sparticle | $\sqrt{s} = 500$ GeV | $\sqrt{s} = 1$ TeV |
|-----------|----------------------|---------------------|
| $\tilde{e}_L$ | 0 | 37 | 63 | 142 |
| $\tilde{e}_R$ | 0 | 72 | 53 | 223 |
| $\tilde{\tau}_1$ | 2 | 142 | 165 | 338 |
| $\tilde{\tau}_2$ | 0 | 11 | 9 | 69 |
| $\tilde{\nu}_e$ | 0 | 42 | 64 | 146 |
| $\tilde{\nu}_\tau$ | 0 | 85 | 81 | 236 |
| $\tilde{\chi}_1^0$ | 26 | 507 | 587 | 626 |
| $\tilde{\chi}_2^0$ | 4 | 397 | 352 | 557 |
| $\tilde{\chi}_3^0$ | 0 | 136 | 57 | 357 |
| $\tilde{\chi}_4^0$ | 0 | 5 | 5 | 66 |
| $\tilde{\chi}_1^\pm$ | 25 | 467 | 505 | 608 |
| $\tilde{\chi}_2^\pm$ | 0 | 17 | 16 | 170 |
| $\tilde{g}$ | 0 | 0 | 27 | 5 |
| $\tilde{d}_L$ | 0 | 3 | 73 | 24 |
| $\tilde{d}_R$ | 1 | 18 | 63 | 157 |
| $\tilde{u}_L$ | 0 | 5 | 81 | 24 |
| $\tilde{u}_R$ | 0 | 14 | 86 | 79 |
| $\tilde{b}_1$ | 0 | 20 | 103 | 189 |
| $\tilde{b}_2$ | 0 | 0 | 3 | 4 |
| $\tilde{t}_1$ | 1 | 2 | 94 | 58 |
| $\tilde{t}_2$ | 0 | 0 | 0 | 0 |

Table 8: Same as the previous Table but now corresponding to the 672(663) undetected flat(log) prior models assuming $\mathcal{L} = 10$ fb$^{-1}$ with $\delta B = 20\%$. 
for charginos, stops, sbottoms, selectrons (or smuons) and staus in the flat prior model set is seen to decrease significantly as the LHC accumulates integrated luminosity without observation of a signal for SUSY. However, note that for the corresponding log prior model set, while the number of surviving models decreases with any corresponding increase in the LHC integrated luminosity (or with any decrease in the SM background uncertainty) as one would expect, the fraction of the surviving models with a kinematically accessible sparticle changes very little, if at all! For charginos at a 500 GeV LC this fraction is found to be quite large, \( \sim 75\% \), but it is found to be somewhat smaller for the other sparticles, e.g., \( \sim 25\% \) for \( \tilde{\tau}_1 \) and \( \sim 7\% \) for \( \tilde{e}_L \).

One possible explanation of this unexpected behavior in the log prior sample is as follows: As we saw in the previous discussion of fine-tuning, in the log prior case, the removal of pMSSM models from the log prior set (as they are ‘discovered’ by ATLAS) must affect the various sparticle mass distributions in a roughly uniform manner. Otherwise the observed amount of fine-tuning would necessarily increase. However, in the flat prior case, models with lighter sparticles are preferentially ‘discovered’ by ATLAS searches. This hypothesis can qualitatively explain why there is no significant reduction in the fraction of the log prior models with kinematically accessible sparticles at a 500 GeV (or 1 TeV) LC (especially in the case of non-colored sparticles as we have seen above). It also simultaneously explains why the apparent amount of fine-tuning does not change appreciably as the LHC covers more of the log scan parameter space. Of course, as can be seen from these figures, at a 1 TeV LC a substantial portion of both the log and flat prior model sets which remain undiscovered at the LHC have sparticles which are kinematically accessible even at high LHC integrated luminosities. We further note that the fraction of LHC-unobserved models where no SUSY sparticles whatsoever are accessible at a LC (not even the LSP) is quite large for the flat model set at a 500 GeV LC, but is only in the 12-20% range for the corresponding log prior model set. On the other hand, at a 1 TeV LC, this value is seen to lie below \( \sim 1\% \) for the log prior models, while for the flat prior set it remains below \( \sim 13\% \). Clearly, a 1 TeV LC will be far better at accessing the sparticles in our pMSSM model sets.

In order to test this hypothesis, we show the mass distributions for the \( \tilde{e}_L \) and \( \tilde{\chi}^0_2 \) in both the flat and log prior model sets in Fig. 25\footnote{Note that there is nothing special about the choice of these two particular non-colored sparticles and the features that we will now describe are also found in the mass distributions of other sparticles.}. Indeed, we see that this hypothesis is true for non-colored states: in the flat prior set, models being observed by the ATLAS analyses mostly correspond to those with lower sparticle masses. On the other hand, for the log prior case, we see that the mass distributions for non-colored sparticles approximately maintain their overall shape as the models are observed, showing not much preference for the lighter sparticle masses. Fig. 26 shows, however, that in the case of colored sparticles, here for the gluinos and (one of the) squarks, which are most directly sensitive to most of the ATLAS \( E_T^{\text{miss}} \) analyses, this same effect is somewhat less significant. In particular for the gluinos we see that even in the log prior case there is a significant loss in the fraction of models with lighter masses as the LHC integrated luminosity is increased.
Figure 23: Top left: Fractional number of undetected models with kinematically accessible $\tilde{\chi}_1^\pm$ at a 500 GeV LC as a function of the LHC integrated luminosity for flat(solid) and log(dashed) prior models. The red(green, blue) curves correspond to background systematic uncertainties of 50(100,20)%, respectively. Bottom left: Same as the previous panel but now for flat prior models only with $\delta B = 50\%$ for the $\tilde{\tau}_1$(blue), $\tilde{e}_R$(green), $\tilde{e}_L$(red), $\tilde{t}_1$(solid) and $\tilde{b}_1$(magenta). Bottom right: Same as the previous panel but now for log prior models. Top right: Fraction of undetected models with no sparticles kinematically accessible. The magenta(green,blue) curves are for log prior models with $\delta B = 20(50,100)\%$ while the blue(red,cyan) curves are the corresponding results for the flat prior set.
Figure 24: Same as in the previous Figure but now for a 1 TeV LC.
Figure 25: Mass distributions for $\tilde{e}_L$(top) and $\tilde{\chi}^0_2$(bottom) for the ATLAS-undetected flat(left) and log(right) prior models assuming $\delta B = 50\%$ for different values of the LHC integrated luminosity as indicated. The top red histogram in each case corresponds to the original model sets before any of the ATLAS analyses are considered while the subsequently lower histograms correspond to those subsets of models undetected by the ATLAS $E_T^{\text{miss}}$ analyses at fixed integrated luminosities.
Figure 26: Same as the previous Figure but now for gluinos and $\tilde{u}_L$. 
5 Summary and Conclusions

In this paper we have analyzed the capability of the ATLAS $E_T^{\text{miss}}$-based SUSY analyses to discover Supersymmetry in a model independent fashion at the 7 TeV LHC. To this end, we tested these search channels on a large set of model points, $\sim 71k$, in the 19-dimensional parameter space of the pMSSM. This model sample contains a wide variety of properties and characteristics and provides a framework to explore the breadth of possible SUSY signatures at colliders and elsewhere. These models were generated in a previous work and comply with a set of minimal theoretical assumptions as well as the global precision electroweak, heavy flavor, collider searches, and astrophysical data sets. We simulated ten ATLAS $E_T^{\text{miss}}$ search channels, which were designed in the context of mSUGRA-based SUSY, and employed the SM backgrounds as provided directly by the ATLAS SUSY working group. We first checked that our analyses were in agreement with ATLAS results for the mSUGRA benchmark point that the collaboration had previously simulated.

We passed our model sample through the ATLAS analysis chain and computed the significance of the signal for each model in each search channel. A significance of $S \geq 5$ was used as the criteria for discovery in each channel; we employed the same numerical technique that ATLAS does for calculating this value. We found that the systematic error due to uncertainties in the size of the expected background made a substantial impact on model discovery for the range of expected integrated luminosities. In fact, some channels become systematics dominated at luminosities of order $5 - 10 \, \text{fb}^{-1}$. Overall, for $1(10) \, \text{fb}^{-1}$ of integrated luminosity roughly 80(95)% of the flat prior model sample is discoverable, assuming a 50% background systematic error. Larger (or smaller) systematic errors greatly reduce (or increase) this model coverage. We found that the 4j0l channel is the most powerful in terms of observing a signal, whereas the leptonic channels had a much reduced model coverage. This is due to the suppression of leptonic cascade decays appearing in our model sample compared to expectations from e.g., mSUGRA. The model coverage was worse for the log prior sample due to kinematic reasons.

We explored the characteristics that caused a model to not be observed in these search channels. While production cross section values as related to the sparticle mass obviously plays a role, it does not tell the whole story. There are cases with low mass gluinos and/or squarks with large cross sections that are missed by these search analyses, while models with heavy masses and small cross sections are sometimes observed. We found that the mass splitting between the gluino/squarks and the LSP plays an important role in detecting models, and that this can sometimes be compensated by very large production rates or ISR. We also saw that subtleties in the sparticle spectrum can conspire to render a model to not be detected. A fraction of our model set contains detector-stable sparticles which appear at the end of their cascade decay chains and hence are not detected by the $E_T^{\text{miss}}$-based searches. We studied the effectiveness of the planned stable charged particle searches in these cases and found that some, but not all, of these models will be discovered.
We briefly considered potential modifications to the ATLAS kinematic cuts in these $E_T^{\text{miss}}$ analyses that would improve their discovery potential. We studied the optimal cut on $M_{eff}$ as well as for the $p_T$ of the leading jet and overall $E_T^{\text{miss}}$. Our results indicate that the cuts for both the leading jet transverse momentum and the $E_T^{\text{miss}}$ could be increased from their nominal value without seriously impacting model coverage.

Lastly, we studied the implications of a null result from the 7 TeV LHC run. We found that the degree of fine-tuning that would be imposed on the pMSSM depended on the choice of priors which generated the model sample, but overall would not be as large as in the case of mSUGRA. However, the expectations for sparticle production at a high energy Linear Collider would be greatly impacted if Supersymmetry is not discovered during this LHC run. Basic kinematics would essentially exclude sparticle production at a 500 GeV Linear Collider, and would point towards the need for a higher energy machine in order to study Supersymmetry.

In summary, we find that the mSUGRA motivated $E_T^{\text{miss}}$-based searches for Supersymmetry perform well over a larger and more complicated SUSY parameter space such as the pMSSM. However, there are some exceptions and coverage is not perfect. The details of the full sparticle spectrum play a very important role in the observability of a model. There are no blanket statements regarding the potential for discovery, or in setting a mass limit, that that can honestly be made.

We anxiously await the discovery of Supersymmetry in the near future.

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