ABSTRACT

It has been well established that Galactic Globular clusters (GCs) harbour more than one stellar population, distinguishable by the anti-correlations of light element abundances (C-N, Na-O, and Mg-Al). These studies have been extended recently to the asymptotic giant branch (AGB). Here we investigate the AGB of NGC 6397 for the first time. We have performed an abundance analysis of high-resolution spectra of 47 RGB and 8 AGB stars, deriving Fe, Na, O, Mg and Al abundances. We find that NGC 6397 shows no evidence of a deficit in Na-rich AGB stars, as reported for some other GCs – the subpopulation ratios of the AGB and RGB in NGC 6397 are identical, within uncertainties. This agrees with expectations from stellar theory. This GC acts as a control for our earlier work on the AGB of M 4 (with contrasting results), since the same tools and methods were used.

Key words: Galaxy: formation – Galaxy: abundances – Galaxy: globular clusters: general – stars: abundances – stars: AGB and post-AGB.

1 INTRODUCTION

It is well known that Galactic globular clusters (GCs) show star-to-star spreads in the abundances of proton-capture elements (primarily He, C, N, O and Na), while most GCs remain homogeneous in the iron peak species (Carretta et al. 2009b). This spread often presents as multi-modal (as in the early low-resolution cyanogen (CN) studies of Norris 1981; Cottrell & Da Costa 1981), with two or more distinct subpopulations being identified. One of these subpopulations is always chemically similar to Galactic halo stars of the same metallicity – designated here as SP1 and which is inferred to contain primordial He abundances – with one or more further subpopulations found to have higher N and Na (and lower C and O) abundances – here designated collectively as SP2 (see Gratton et al. 2012, for an extensive review). These are the ubiquitous C-N and Na-O (and Mg-Al in some GCs) anti-correlations (Carretta et al. 2009a). This spread in light elemental abundance can also be inferred from narrow and intermediate band photometric data, seen as multiple red- or sub-giant branches, or multiple main sequences in a GC’s colour-magnitude diagram (e.g., Milone et al. 2008, 2014).

The peculiar abundance signature of SP2 stars has been observed in both evolved and unevolved stars in many clusters (Gratton et al. 2001), indicating that this pattern is likely to have been inherited at birth. Furthermore, the pattern is generally not observed elsewhere, such as the (less massive) open clusters of the Galaxy (De Silva et al. 2009; MacLean et al. 2015); however very recently it has been suggested that the Galactic bulge may contain SP2-like stars (Schiavon et al. 2017). The most common explanation for this light-elemental inhomogeneity is the self-pollution hypothesis where the ejecta of more massive SP1 stars mixed with an early dense interstellar medium, from which SP2 stars were formed (Cannon et al. 1998; Gratton et al. 2004).

Importantly, the relative fractions of each subpopulation remain the same through all these phases of evolution, as expected from stellar evolutionary theory. However, un-
til recently there were no systematic surveys of asymptotic giant branch (AGB) stars. Some early (e.g., Norris et al. 1981) and more recent (Campbell et al. 2010, 2013) low-resolution spectroscopic studies of GCs found that the distribution of cyanogen band strengths varies greatly between the RGB and AGB of several GCs. In particular, they found no CN-strong (i.e., SP2) AGB stars in NGC 6752, which has an extended blue horizontal branch (HB). These results hinted at differences in evolution between stars of different light elemental abundances, which are not fully predicted in standard stellar evolution theory – only stars with extreme He abundances are expected to avoid the AGB phase due to smaller envelopes in the HB phase (Dorman et al. 1993; Campbell et al. 2013; Cassisi et al. 2014).

In this paper we use the prescription as described in MacLean et al. (2016, hereafter ML16), where the percentages of RGB and AGB stars in a GC that are found to be members of SP2 are written as $R_{RGB}$ and $R_{AGB}$, respectively (typical $R_{RGB}$ values are $\sim$50-70%; Carretta et al. 2010); and the SP2 AGB deficit is given by

$$F = (1 - \frac{R_{AGB}}{R_{RGB}}) \times 100\%,$$

where a value of 100% indicates that no SP2 stars reach the AGB – as reported for NGC 6752 and M 62 by Campbell et al. (2013) and Lapenna et al. (2015), respectively. For clusters with extended HBs (where the bluest stars reach $T_{eff}$ over 15,000 K; e.g., NGC 6752, NGC 2808), an $R_{AGB}$ value of up to $\sim$30% may be expected due to the well-established existence of AGB-manqué stars (which evolve directly from the HB to the white dwarf phase, avoiding the AGB; Greggio & Renzini 1990; Dorman et al. 1993; Cassisi et al. 2014). Clusters whose HBs do not extend into this regime (e.g., M 4, NGC 6397) are expected to have an $F$ value of zero per cent, with all stars in the cluster ascending the AGB.

There has been much debate as to the level and existence of GC SP2 AGB deficits in recent years as more evidence has been gathered, but a definitive conclusion has yet to be reached. In fact, contradictory evidence has been gathered, but a definitive conclusion – establishment of AGB-manqué stars (which evolve directly to the white dwarf phase (AGB-manqué stars). SP2 AGB deficits above $F \approx 30\%$ suggest that the location along the HB where this alternative evolutionary path begins to occur may be incorrectly predicted by theory, and/or dependent on more factors than previously thought.

Similar to the debate on AGB abundances in NGC 6752, recent studies on the archetypical GC M 4 have presented starkly different conclusions on the nature of its AGB. ML16 presented [Na/Fe] and [O/Fe] abundances for both AGB and RGB stars in M 4, reaching the conclusion that all AGB stars are consistent with being SP1 stars (i.e., $F \approx 100\%$). In contrast, Lardo et al. (2017) and Marino et al. (2017) – using photometric indices and spectroscopic analysis, respectively – concluded that the spread of light elemental abundances in the AGB of M 4 is similar to the RGB (however, both studies found that their AGB samples were offset toward SP1-like abundances). If true, this is consistent with the theoretical prediction of $F = 0\%$. However, the very recent study of Wang et al. (2017) showed that the spread in Na abundances of M 4’s AGB is significantly narrower than the RGB, qualitatively similar to the findings of ML16, but not as extreme. It is clear that further study of this GC is required.

If high SP2 AGB deficits are reliably demonstrated, this may impose new and important restrictions on low-mass, low-metallicity stellar evolution and/or atmospheric models; impacting the field of globular clusters, stellar evolution, and Galactic formation and archaeology.

In the current study we aim to derive AGB subpopulation ratios for the GC NGC 6397 for the first time. NGC 6397 is an old and metal-poor GC with a well-documented Na-O anti-correlation on the RGB, the range of which is smaller than many other clusters (no ‘extreme population’ in the classification of Carretta et al. 2009b, which is associated with high He abundance). NGC 6397 also displays a Mg-Al anti-correlation (Lind et al. 2011a, hereafter L11). The short (but blue) HB of NGC 6397 extends between 8000K $< T_{eff}$ $< 10,500K$, suggesting that no stars in the cluster should evolve into AGB-manqué stars (Lovisi et al. 2012). In order to determine if this is the case, we have performed an analysis of spectra from a sample of AGB and RGB stars in NGC 6397. For each star we have derived radial velocities, stellar parameters, and abundances of Fe, Na, O, Mg and Al.

2 SAMPLE SELECTION, OBSERVATIONS AND MEMBERSHIP

Our stellar targets were selected from the NGC 6397 photometric dataset of Momany et al. (2003, UBVI from the ESO/MPG WFI, see Table 1). For the bright stars considered here the photometric completeness is 100%, for all colours. The photometry covers the entire cluster out to at least 9 arcmin from the cluster centre (in some directions reaching to $\sim$22 arcmin). This compares with the cluster’s half-light radius of 2.9 arcmin (Harris 1996). To avoid crowding problems in the core with multi-object fibre placement the sample was limited to stars outside $\sim$0.5 arcmin of the cluster centre.

The RGB and AGB are separated in $V-(B-V)$ and
U − (U−I) space (Figure 1). AGB stars were conservatively selected – only early-AGB stars were included so as to avoid the mislabelling of stars since the AGB and RGB colours become similar at brighter magnitudes. We then cross-matched our selection with the 2MASS database to take advantage of the high quality astrometry and JHK photometry. 2MASS IDs and JHK photometric magnitudes for the whole sample are included in Table 1. In total our initial target sample included 9 AGB stars and 64 RGB stars. Importantly for the science goal of this study the RGB and AGB samples are spatially coincident.

High-resolution spectra were collected in July 2015 using 2dF+HERMES on the Anglo-Australian Telescope which provides \( R = 28,000 \) spectra in four narrow windows; blue (4715 - 4900 Å), green (5649 - 5873 Å), red (6478 - 6737 Å), and infrared (7585 - 7887 Å) (for more details on the HERMES instrument, see De Silva et al. 2015; Sheinis et al. 2015). Due to restrictions on 2dF fibre positioning, we were able to collect spectra for only 60 of the 73 targets. This down-sampling is random, except that priority was given to obtaining the largest possible sample of AGB stars, since the number of AGB stars is inherently low compared to RGB stars (see Fig 1, black dots). In total we collected spectra for 8 of the 9 identified AGB stars, and 52 RGB stars.

The spectra had an average signal-to-noise ratio of 70. The software package 2dFdr (AAO Software Team 2015, v6.5) was used to reduce the data for analysis. Radial velocities were measured with the IRAF fxcor package (Tody 1986), using a solar reference template. The mean radial velocity for NGC 6397 after non-member elimination was found to be \( \langle v_r \rangle = 19.30 \pm 0.48 \) km/s (\( \sigma = 3.71 \) km/s), consistent with Lind et al. (2009), who report \( \langle v_r \rangle = 18.59 \pm 0.16 \) km/s (\( \sigma = 3.61 \) km/s). Individual stellar radial velocities are listed in Table 1. Iterative 3-\( \sigma \) clipping of radial velocities and metallicities (discussed in §3.2) reduced the final RGB sample to 47 stars. All of the 8 observed AGB stars were found to be members.

Apart from not sampling the inner core of the cluster we do not identify any sample bias. Moreover we have collected spectra for almost all of the AGB stars in the very wide field of view of the source photometry. The 47 RGB stars offer a solid basis for comparison. The final observed samples can be seen visually in the colour-magnitude diagrams of Figure 1, over-plotted against the full photometry sample.

3 METHOD
3.1 Atmospheric parameters

For this study we have used several photometric relations to determine effective temperatures for all stars.

Typically with spectroscopic studies (such as ML16), stellar parameters are determined by requiring the excitation and ionisation balance of abundances from neutral and singly-ionised iron (Fe i & Fe ii, respectively) absorption lines (e.g., Sousa 2014). While a significant strength of this method is that the parameters are unaffected by photometric reddening, there are also many weaknesses. Many solutions can be found for a single star, largely depending on the choice of initial parameter estimates (see C17). Additional spectroscopic uncertainties such as EW measurements, choice of atmospheric model, atomic line data, and parameter interdependence can compound this problem.

To further complicate the picture, Lapenna et al. (2014, 2016) have provided evidence that the Fe i lines of AGB stars may experience a higher degree of non-LTE effects than RGB stars at the same metallicity and effective temperature. If true, then assuming ionisation balance may artificially and preferentially lower the derived surface gravity of AGB stars (Lind et al. 2012). In C17 we suggested that this so-called ‘AGB iron over-ionisation problem’ does not exist (at least in NGC 6752), but may be the result of systematic offsets in photometrically-derived \( T_{\text{eff}} \). Regardless, Fe i lines are well known to experience some non-LTE effects (on both the RGB and AGB, and especially at low metallicities, see Bergemann et al. 2012), so forcing ionisation balance prior to the correction of non-LTE effects may result in systematically incorrect gravities and metallicities in all stars.

We have used the B−V and V−K relations from Ramírez & Meléndez (2005), González Hernández & Bonifacio (2009) and Casagrande et al. (2010) to determine \( T_{\text{eff}} \) estimates.
Momany et al. (2003, June 2014 release) and model atmospheres (2014). We adopt Miglio et al. 2016 6 and Lovisi et al. 2012 Gratton et al. 2012 (2; Castelli & Kurucz 2003 Lind et al.). NGC 6397 does not suffer Table 1. NGC 6397 target details including data from Momany et al. (2003, UBVI photometry and target IDs) and 2MASS (Skrutskie et al. 2006, JHK photometry – gaps in data represent targets with low quality flags), radial velocities (km/s), and Lind et al. (2011a, L11) IDs. Full table available online.

| ID          | Type | 2MASS ID                | L11 ID | V Mag | B Mag | U Mag | I Mag | J Mag | H Mag | K Mag | RV (km/s) |
|-------------|------|-------------------------|--------|-------|-------|-------|-------|-------|-------|-------|-----------|
| 56897       | AGB  | 17400665-5335001        | -      | 11.83 | 12.76 | 10.59 | 13.11 | 9.76  | 9.25  | 9.13  | 17.17     |
| 60099       | AGB  | 17402547-5347570        | -      | 11.65 | 12.62 | 10.37 | 12.97 | -     | -     | -     | 20.68     |
| 70509       | AGB  | 17405254-5341049        | -      | 11.98 | 12.90 | 10.75 | 13.17 | 9.95  | 9.48  | 9.31  | 19.38     |
| 70522       | AGB  | 17404076-5341046        | -      | 11.16 | 12.24 | 9.79  | 12.80 | 8.94  | 8.37  | 8.26  | 18.93     |
| 73216       | AGB  | 17403510-5339572        | -      | 11.83 | 12.76 | 10.57 | 13.11 | -     | -     | -     | 16.00     |

Table 2. Average differences in $T_{eff}$ between the adopted value and each photometric estimate. Uncertainties are the 1σ standard deviations of the cluster samples. The average σ value in the last row is indicative of the spread of $T_{eff}$ estimates for each star.

| Method      | $\Delta T_{eff}$ (K) |
|-------------|-----------------------|
| Ram (B−V)   | 94 ± 45               |
| Gonz (B−V)  | −17 ± 42              |
| Casa (B−V)  | 22 ± 98               |
| Ram (V−K)   | 69 ± 35               |
| Gonz (V−K)  | −34 ± 34              |
| Casa (V−K)  | −33 ± 32              |
| IRFM        | −108 ± 47             |

Average σ ± 48

1Ramírez & Meléndez (2005) 2González Hernández & Bonifacio (2009) 3Casagrande et al. (2010)

Additionally, we have calculated $T_{eff}$ without relying on colour calibrations, by implementing the infrared flux method (IRFM) at an estimated log $g$ of each AGB and RGB star, as described in Casagrande et al. (2010, 2014) using BVI and 2MASS JHK photometry. Thus we have seven $T_{eff}$ estimates for each star. These methods are dependent on metallicity, for which a value of [Fe/H] = −2.00 was assumed for NGC 6397. To account for interstellar extinction we applied a constant correction of $E(B−V)$ = −0.19 to all stars (Gratton et al. 2003). NGC 6397 does not suffer from significant differential reddening (Milone et al. 2012).

Four stars were flagged for low quality and/or contamination in the 2MASS database so only the B−V relations were used to determine $T_{eff}$ for these stars. For all other stars, the mean of the seven $T_{eff}$ estimates was adopted. Table 2 shows the variation between the final adopted $T_{eff}$ values and those of the photometric relations and IRFM. Surface gravities ($\log g$) and micro-turbulences ($\nu_t$) were determined using the empirical relations from Alonso et al. (1999) and Gratton et al. (1996), respectively, and assuming a mass of 0.8 $M_\odot$ and 0.7 $M_\odot$ for the RGB and AGB, respectively (Lovisi et al. 2012, Miglio et al. 2016). We adopt a 1σ uncertainty of ±50K for $T_{eff}$ (see Table 2), ±0.1 dex for $\log g$, and ±0.2 km/s for $\nu_t$. Final stellar parameters for each star are included in Table 5 and represented visually in Figure 2.

3.2 Chemical abundance determination

Chemical abundances were determined for Fe (using Fe i and Fe ii), Na (Na i), O (O i), Mg (Mg i), and Al (Al i) using the equivalent width (EW) method. EWs of absorption lines were measured using a combination of the ARES (Sousa et al. 2015, v2) and IRAF onedspec packages, while one-dimensional LTE abundances were determined using the MOOG code (Sneden 1973, June 2014 release) and model atmospheres that were interpolated from the Castelli & Kurucz (2004) grid. The line list and atomic data used for this analysis are specified in Table 3. The LTE assumption has been known for many years to be an inaccurate approximation for the abundances of many elemental species. In fact, all elements determined in this work are affected by non-LTE effects which must be accounted for if the abundances are to be reliable. Fortunately, grids of non-LTE corrections now exist for all of these elements in the parameter space occupied by our stellar sample.

Iron abundances determined from neutral absorption lines are known to be systematically lower than those determined using singly-ionised lines (for which LTE is a realistic approximation; Lind et al. 2012). However, due to the large number of Fe lines in a stellar spectrum, it can prove difficult to perform a complete line-by-line non-LTE analysis using published grids. For this reason, we performed a test to gauge the magnitude of the offsets on a subset of stars and
lines. For our test, we selected a representative sub-sample of three RGB and three AGB stars from NGC6397, and interpolated corrections from Amarsi et al. (2016b) for five Fe I lines\(^1\) and two Fe II lines\(^2\). The results of this test are summarised in the first two rows of Table 4. We did not apply these average corrections, but compare them to our LTE Fe results in Section 4.

Non-LTE corrections were applied to all Na, O, Mg, and Al abundances line-by-line using the most recent grids. As in ML16, Na abundances were determined using the 568 nm doublet and corrected for non-LTE effects as described in Lind et al. (2011b) by using the web-based INSPECT interface\(^3\), and adopting the provided \(\Delta[\text{Na}/\text{Fe}]_{\text{NLTE}}\) corrections. The oxygen 777 nm triplet was measured and non-LTE corrections were determined by the interpolation of the recent Amarsi et al. (2016a) grid of corrections. For Mg, the measured EWs of the 571 nm and 769 nm lines were used for non-LTE determinations as described in Osorio & Barklem (2016), using the INSPECT interface. The average of these two values was then used to correct the 473 nm Mg line. Finally, both the 669 nm and 783 nm doublets were used to determine Al abundances, while non-LTE adjustments were interpolated from the new results of Nordlander & Lind (2017). Average non-LTE corrections, and associated spreads are listed in Table 4.

### 4 ABUNDANCE RESULTS & ANALYSIS

Final elemental abundances are presented in Table 5. Uncertainties cited in the table are based only on the line-to-line scatter of each abundance and do not consider additional sources of error. Using our estimated 1\(\sigma\) uncertainties of each stellar parameter (±50K in \(T_{\text{eff}}\), ±0.1 in log \(g\), ±0.2 km/s in \(v_\text{t}\)), an atmospheric sensitivity analysis was performed on a representative sub-sample and results are summarised in Table 6. Finally, in Table 7 we present a summary of all identified sources of uncertainties and adopted total abundance uncertainties.

A comparison of our results was made with that of Lind et al. (2011b, L11) and Carretta et al. (2009a, C09), with which we had a total of 5 and 21 RGB stars in common, respectively. The results of the detailed comparison of all stellar parameters and abundances are presented in Table 8, which shows good agreement in all stellar parameters and slight to moderate offsets in abundance results (0.03 to 0.18 dex) between the studies. These offsets arise from different methods in analysis.

In the cases of assumed stellar mass, atmospheric model parameters, adopted non-LTE corrections, and adopted solar abundances, we were able to quantify the effects since the previous studies published their values for these inputs. These sources of uncertainty combine to total possible offsets of up to ±0.10 dex in each abundance. Other sources of uncertainty which we could not quantify (because we do not have the relevant information from the related studies)

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1. 4788.8 Å, 4839.5 Å, 5701.6 Å, 5753.1 Å and 7748.3 Å
2. 6516.1 Å and 7711.7 Å
3. http://inspect-stars.net

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**Table 3.** Adopted line list used for EW measurements. Based on the line list of the GALAH collaboration (De Silva et al. 2015).

| Wavelength (Å) | Species | Excitation Potential (eV) | \(\log gf\) |
|----------------|--------|--------------------------|-------------|
| 7711.94        | O i    | 9.146                    | 0.369       |
| 7774.16        | O i    | 9.146                    | 0.225       |
| 7775.39        | O i    | 9.146                    | 0.002       |
| 5682.63        | Na i   | 2.100                    | −0.706      |
| 5688.20        | Na i   | 2.100                    | −0.404      |
| 4730.03        | Mg i   | 4.350                    | −2.347      |
| 5711.09        | Mg i   | 4.350                    | −1.724      |
| 7691.53        | Mg i   | 5.750                    | −0.783      |
| 6696.02        | Al i   | 3.140                    | −1.569      |
| 6698.67        | Al i   | 3.140                    | −1.870      |
| 7835.31        | Al i   | 4.020                    | −0.689      |
| 7836.13        | Al i   | 4.020                    | −0.534      |
| 4788.76        | Fe i   | 3.237                    | −1.763      |
| 4839.54        | Fe i   | 3.270                    | −1.820      |
| 4890.75        | Fe i   | 2.875                    | −0.394      |
| 4891.49        | Fe i   | 2.849                    | −0.111      |
| 5701.56        | Fe i   | 2.559                    | −2.220      |
| 5753.12        | Fe i   | 4.260                    | −0.690      |
| 5859.59        | Fe i   | 4.549                    | −0.419      |
| 5862.36        | Fe i   | 4.549                    | −0.127      |
| 6498.94        | Fe i   | 0.958                    | −4.687      |
| 6518.37        | Fe i   | 2.831                    | −2.440      |
| 6592.91        | Fe i   | 2.727                    | −1.473      |
| 6593.87        | Fe i   | 2.433                    | −2.420      |
| 6609.11        | Fe i   | 2.559                    | −2.691      |
| 6677.99        | Fe i   | 2.690                    | −1.420      |
| 7748.27        | Fe i   | 2.949                    | −1.751      |
| 7780.56        | Fe i   | 4.473                    | −0.010      |
| 4731.45        | Fe ii  | 2.891                    | −3.100      |
| 6516.08        | Fe ii  | 2.891                    | −3.310      |
| 7711.72        | Fe ii  | 3.903                    | −2.500      |

**Table 4.** Summary of average non-LTE corrections for each element, with 1\(\sigma\) standard deviations over the stellar sample.

| Species | Average Non-LTE Correction |
|---------|-----------------------------|
|         | RGB                        | AGB                        |
| Fe i    | +0.08 ± 0.04               | +0.08 ± 0.03               |
| Fe ii   | <0.01                      | <0.01                      |
| O       | −0.05 ± 0.01               | −0.06 ± 0.01               |
| Na      | −0.06 ± 0.02               | −0.06 ± 0.01               |
| Mg      | +0.02 ± 0.01               | +0.02 ± 0.01               |
| Al      | −0.06 ± 0.03               | −0.05 ± 0.05               |

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1. For example different line lists, EW measurements and instrumentation differences – most likely explain the remaining offsets. We note that the scatter around these offsets is typically considered a better indication of the agreement between abundance analysis studies, and is consistent with the uncertainties quoted in this work. We find very good agreement between our study and that of L11. A curiosity here is the lack of agreement on micro-turbulence values with C09. While we adopted photometric \(v_\text{t}\) (and therefore had a relatively small spread in values, ranging from 1.52 km/s to 1.71 km/s), C09 determined micro-turbulence spectroscopically and had a very large spread in \(v_\text{t}\) values (ranging from 0.11 km/s to 2.73 km/s in the overlapping sample). This
Table 5. Stellar parameters, and derived chemical abundances for each star in NGC6397. Abundance uncertainties reflect line-to-line scatter (1σ), and do not take atmospheric sensitivities into account (see Table 6, and text for discussion). The last two rows are the cluster average abundances with error on the mean, and standard deviation to indicate observed scatter. We adopt the Asplund et al. (2009) solar abundance values. The full table is available online.

| ID     | Type | Teff (K) | log g (cgs) | v_t (km/s) | [Fe/H] | [Fe/H] | [O/H] | [Na/H] | [Mg/H] | [Al/H] |
|--------|------|----------|-------------|------------|--------|--------|-------|--------|--------|--------|
| 56897  | AGB  | 4978     | 1.80        | 1.64       | -2.13 ± 0.06 | -2.00 ± 0.02 | -1.64 ± 0.01 | -1.92 ± 0.01 | -1.84 ± 0.04 | -1.32 ± 0.05 |
| 60699  | AGB  | 4905     | 1.70        | 1.67       | -2.23 ± 0.07 | -2.06 ± 0.01 | -1.45 ± 0.04 | -1.98 ± 0.01 | -2.02 ± 0.01 | -1.37 ± 0.01 |
| 70599  | AGB  | 5017     | 1.80        | 1.61       | -2.18 ± 0.06 | -2.07 ± 0.04 | -1.49 ± 0.04 | -2.15 ± 0.01 | -1.79 ± 0.05 | -1.53 ± 0.04 |
| 70522  | AGB  | 4739     | 1.42        | 1.76       | -2.24 ± 0.05 | -2.06 ± 0.03 | -1.63 ± 0.02 | -1.94 ± 0.04 | -1.99 ± 0.08 | -1.48 ± 0.06 |
| 73216  | AGB  | 4968     | 1.80        | 1.64       | -2.16 ± 0.05 | -2.04 ± 0.00 | -1.39 ± 0.06 | -2.29 ± 0.04 | -1.73 ± 0.05 | -1.67 ± 0.03 |

Mean σ

| | -2.15 ± 0.01 | -2.02 ± 0.00 | -1.52 ± 0.02 | -2.06 ± 0.02 | -1.87 ± 0.01 | -1.49 ± 0.02 |

Table 6. Typical abundance uncertainties due to the (1σ) atmospheric sensitivities of a representative sub-sample of three RGB and two AGB stars in our NGC6397 data set. Parameter variations (in parentheses) are the expected uncertainties in the respective parameters.

| Parameter | This study - L11 | This study - C09 |
|-----------|------------------|------------------|
| ∆Teff (±50 K) | -4.3 ± 20.9 | 19.5 ± 29.9 |
| ∆log g (±0.1 dex) | 0.08 ± 0.01 | 0.07 ± 0.02 |
| ∆v_t (±0.2 km/s) | 0.04 ± 0.03 | 0.21 ± 0.64 |
| [Fe/H] | -0.08 ± 0.03 | -0.13 ± 0.05 |
| [Fe/H] | 0.12 ± 0.03 | 0.05 ± 0.05 |
| [O/H] | 0.06 ± 0.08 | 0.18 ± 0.14 |
| [Na/H] | -0.03 ± 0.06 | -0.17 ± 0.14 |
| [Mg/H] | -0.09 ± 0.03 | - |
| [Al/H] | 0.17 ± 0.12 | - |

dex, see [§3.2 and Fig 3]. While this could indicate slight systematics in either our Teff estimates or the non-LTE corrections, the uncertainty range of our <δFe> value overlaps with that of the non-LTE predicted δFe value, indicating broad agreement. Our Fe abundances are consistent with literature values (δ[Fe/H]>L11 = -2.08 ± 0.02). Furthermore, the difference between the average RGB and AGB δFe values is less than 0.015 dex for NGC6397, indicating that there are no significant offsets in 4Fe between the two giant branches, as has been disputed for NGC6752 (Lapenna et al. 2016; Campbell et al. 2017). This is presented visually in Figure 3, where the overall homogeneity of Fe abundances can be seen, especially between the AGB and RGB.

Abundances of elements other than iron are presented in Tables 5 and 6. The abundance distributions of the two giant branches in NGC6397 are remarkably similar – we find that $\delta_{\text{RGB}} \simeq \delta_{\text{RGB}} \simeq 60\%$ (compared with $\delta_{\text{RGB}} \simeq 75\%$ in L11), indicating no significant offsets in δFe between the two giant branches, as has been disputed for NGC6752 (Lapenna et al. 2016; Campbell et al. 2017). This is presented visually in Figure 3, where the overall homogeneity of Fe abundances can be seen, especially between the AGB and RGB.

Abundances of elements other than iron are presented in Figures 4, 5, and 6. NGC6397 was shown by L11 to have both Na-O and Mg-Al anti-correlations, which we find on both the RGB and AGB, along with a Na-Al correlation (Fig 6). The abundance distributions of the two giant branches in NGC6397 are remarkably similar – we find that $\delta_{\text{RGB}} \simeq \delta_{\text{RGB}} \simeq 60\%$ (compared with $\delta_{\text{RGB}} \simeq 75\%$ in L11), indicating no significant offsets in δFe between the two giant branches, as has been disputed for NGC6752 (Lapenna et al. 2016; Campbell et al. 2017). This is presented visually in Figure 3, where the overall homogeneity of Fe abundances can be seen, especially between the AGB and RGB.
AGB stars in NGC 6397

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Figure 3. LTE Fe abundances for our NGC 6397 sample. Here, δFe ([Fe i/H] − [Fe ii/H]) is plotted against [Fe ii/H] abundance to highlight departures from LTE in Fe i, and the similarity between the Fe abundances of the AGB and RGB. The error bars indicate typical 1σ total uncertainties on individual abundances (see Table 7), while the black dashed line represents the sample average δFe value of −0.14 dex. The green dashed line represents the expected δFe value (−0.08 dex) from our non-LTE test (see §3.2) and the shaded region indicates the non-LTE uncertainties quoted in Amarsi et al. (2016b, ±0.05 dex).

Figure 4. Na and O abundances for our NGC 6397 sample. The error bars indicate typical 1σ total uncertainties on individual abundances (see Table 7).

NGC 6397, due to a HB that only extends to $T_{\text{eff}} \simeq 10,500$ K (Greggio & Renzini 1990; Dorman et al. 1993; Lovisi et al. 2012).

Finally, in Figure 7, we present Gaussian kernel density estimations (KDEs) of our NGC 6397 [Na/H] abundances, along with those of Lind et al. (2011a, L11) and Carretta et al. (2009a, C09), with systematic offsets removed (see text for details). A smoothing bandwidth of 0.06 dex (total Na uncertainty, see Table 7) was applied to each of our RGB and AGB data sets, while for C09 we used a bandwidth of 0.11 dex, matching their total error calculations (see C09, Appendix A). L11 did not quote total abundance uncertainties, however their average measurement uncertainty in Na was the same as in our sample (0.04 dex), therefore we applied an identical bandwidth of 0.06 dex. The discrepancy between the relative heights of the two peaks in the L11 sample, compared to those of the other samples, may be due to the low number of stars observed in L11 (21 RGB stars).

Figure 5. Same as Figure 4, but for Mg and Al.

Figure 6. Same as Figure 4, but for Na and Al.

Figure 7. Gaussian kernel density estimations (KDEs) of our NGC 6397 [Na/H] abundances, along with those of Lind et al. (2011a, L11) and Carretta et al. (2009a, C09), with systematic offsets removed (see text for details). A smoothing bandwidth of 0.06 dex (total Na uncertainty, see Table 7) was applied to each of our RGB and AGB data sets, while for C09 we used a bandwidth of 0.11 dex, matching their total error calculations (see C09, Appendix A). L11 did not quote total abundance uncertainties, however their average measurement uncertainty in Na was the same as in our sample (0.04 dex), therefore we applied an identical bandwidth of 0.06 dex. The discrepancy between the relative heights of the two peaks in the L11 sample, compared to those of the other samples, may be due to the low number of stars observed in L11 (21 RGB stars).
5 DISCUSSION AND CONCLUSIONS

The primary goal of this study was to determine the proportion of SP2 stars in NGC 6397 that evolve through to the AGB phase. Since the work of Campbell et al. (2013), the nature of AGB stars in GCs has been debated in the literature, with eight high-resolution spectroscopic studies (Johnson et al. 2015; García-Hernández et al. 2015; Lapenna et al. 2015; MacLean et al. 2016; Lapenna et al. 2016; Wang et al. 2016; Marino et al. 2017; Wang et al. 2017) and five photometric studies (Monelli et al. 2013; Milone et al. 2015a, b; Lardo et al. 2017; Gruyters et al. 2017) targeting the AGB directly, along with five theoretical studies seeking to explain the anomalous observations (Charbonnel et al. 2013; Cassisi et al. 2014; Charbonnel et al. 2014; Charbonnel & Chanteau 2016a, b).

Since only HB stars with effective temperatures above \( \sim 15,000 \) K are predicted to evolve directly to the white dwarf phase, the AGBs of clusters that lack an extended blue HB are expected to contain distributions in Na, O, Mg and Al abundances that are statistically indistinguishable from those of the RGB – all cluster stars should evolve through both giant branches (i.e., \( \mathcal{F} \approx 0 \)). Only in clusters with extended blue HBs should the distribution be different, and only with the \( \sim 30 \) per cent most extreme (Na-rich/O-poor/Al-rich) AGB stars missing (i.e., \( \mathcal{F} \approx 30 \% \) Dorman et al. 1993; Cassisi et al. 2014).

Despite a rapidly expanding literature sample of GC AGB studies, the picture is still far from clear. To date, eleven GCs have had their AGB systematically probed with high-resolution spectrographs\(^5\), with mixed results in \( \mathcal{F} \) values (see ML16, Table 4). However, only three clusters have been reported to have \( \mathcal{F} \approx 100 \% \): NGC 6752 (Campbell et al. 2013, C17), M 62 (Lapenna et al. 2015) and M 4 (ML16). Of these, only M 62 has not been disputed by subsequent studies, but we note that this GC has not yet been studied a second time.

Lapenna et al. (2016) reported that the Fe I abundances of AGB stars in NGC 6752 are lower than predicted by standard non-LTE theory. If extrapolated to Na abundance, (i.e., if Na is assumed to follow this trend), the AGB [Na/Fe] abundance distribution moves to be in line with stellar theory (\( \mathcal{F} \approx 30 \% \), as expected in GCs with an extended blue HB), contradicting the conclusions of Campbell et al. (2013) who claimed \( \mathcal{F} \approx 100 \% \). However, in a detailed re-analysis of their data, C17 reported that there was no iron abundance discrepancy in NGC 6752 when more reliable \( T_{\text{eff}} \) scales were used, therefore concluding that the original Na results of Campbell et al. (2013) are reliable. Furthermore, for NGC 6397 we have found no significant \( \delta \text{Fe} \) offset between the AGB and RGB, and that the Fe abundances are internally homogeneous (at the level of our uncertainties). This allows \([X/\text{Fe}]\) abundances to be used for the elemental distribution analyses of the giant branches, because using \([X/\text{Fe}]\) would introduce additional scatter (through measurement uncertainties), but no new information.

The abundances of NGC 6397 (Figs 4-7) contain no evidence of a SP2 AGB deficit, with the relative distributions of the RGB and AGB being identical in all abundance planes (\( \mathcal{F} \approx 0 \% \)).

It is interesting to compare this result with that of M 4 by ML16, since the methods and tools we have used are almost identical. The only difference between the NGC 6397 analysis performed in this study and that of ML16 is the method of determining atmospheric parameters. In ML16, \( T_{\text{eff}}, \log g \) and \( v_t \) values were determined spectroscopically by requiring excitation and ionisation balance (as per Sousa 2014), whereas for NGC 6397 these parameters were estimated through photometric relations. As shown in C17, Na abundances are quite robust, that is they are not as sensitive to systematic shifts in \( T_{\text{eff}} \) as Fe abundances. We have also shown that our Fe results are consistent with non-LTE theory, and show homogeneous abundances in both ionisation states, indicating that our \( T_{\text{eff}} \) scale is accurate. For these reasons, we consider that the different method of parameter determination between our two studies should have little consequence on the reliability of our [Na/H] abundances.

Thus our NGC 6397 result further strengthens the conclusions of ML16 whose analysis was almost identical, but whose results are in contradistinction. We therefore suggest that our original M 4 conclusions (\( \mathcal{F} \approx 100 \), but with some uncertainty) are sound, and that our NGC 6397 results show – by providing a control sample – that our method of analysis does not artificially shift AGB abundances toward SP1-like distributions.

As stated in ML16, our M 4 result (\( \mathcal{F} \approx 100 \)) is in clear contradiction with stellar theory – we can think of no reason why SP2 stars in M 4 should avoid the AGB phase, since the maximum \( T_{\text{eff}} \) of its HB is \( \sim 9000 \) K (Marino et al. 2011). This is especially true in light of our result for NGC 6397 – which has a bluer HB than M 4, but \( \mathcal{F} \approx 0 \% \). In the search for a possible explanation of our results, and those of Campbell et al. (2013, 2017, NGC 6752) and Lapenna et al. (2015, M 62), we consider three possible causes of the low-Na signature of AGB stars in M 4, NGC 6752 & M 62:

(i) The low-Na signature is intrinsic – HB stars are becoming AGB-manqué stars at a much lower HB \( T_{\text{eff}} \) than predicted. This is the most commonly cited explanation in the literature.

(ii) The atmospheric models of some AGB stars are incorrectly determined, but only in particular sections of the GC AGB parameter space. This would result in incorrectly predicted absorption line profiles, and represent a significant ‘blind spot’ in the standard spectroscopic method.

(iii) All Na-rich stars in these three GCs are undergoing an unknown burning or mixing process, between the HB and AGB, that acts to deplete Na in the envelope and leave only a low-Na signature by the early AGB phase.

Investigating these hypotheses is beyond the scope of the present work. However, we note that (iii) is almost certainly impossible since there is no known mechanism that can destroy Na, while simultaneously creating O, in the interior conditions found in these stars.

More generally we note that, of the GCs which have been analysed for SP2 AGB deficits, not a single deficit (or lack thereof) claim has been confirmed by a different working group, or with independently selected targets. This suggests that the methods that are used require detailed investigation and checking, such as performed in C17. This is especially

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5 NGC 2808, NGC 6397, NGC 6752, 47 Tucanae, M 2, M 3, M 4, M 5, M 13, M 55 & M 62
pertinent for M4, for which the three existing studies all give different values of $\psi$. We will aim to resolve this issue in a forthcoming study. Finally, we suggest another potential next step in investigating this problem could be a controlled spectroscopic study of an ‘HB second parameter’ pair or trio of clusters with similar metallicity and age, but different HB morphology (such as NGC 288, NGC 362, and NGC 1851), in an attempt to disentangle the effect of global GC parameters on apparent AGB deficits.

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