Strain Rate and Pressure Effects on Multi-branched Counterflow Flames

Claudia-F. López-Cámara1,*, Albert Jordà Juanós2, William A. Sirignano2
1 Civil and Environmental Engineering, University of California, Irvine, CA 92697, USA
2 Mechanical and Aerospace Engineering, University of California, Irvine, CA 92697, USA

Abstract

This study presents methane-air counterflow simulations, in computationally efficient similar form, allowing combustible mixtures to flow from one or both directions in order to learn more about multi-branched propagating flame structures (e.g., a triple flame). These structures with both premixed and non-premixed flames are commonly seen in more practical combustion analyses. A range of realistic mass mixture fractions and asymmetric chemical rate laws are examined while avoiding the commonly forced unreal symmetric behavior with one-step second-order kinetics. Moreover, a survey of critical parameters is performed varying pressure and normal strain rate to define the flame structure and detect different characters. Three flames can co-exist if the strain rate is low enough and the pressure is high enough. However, at higher strain rate and/or lower pressure, only one or two flames might be obtained. Negative regions of heat release rate are observed and linked to potential endothermic reactions. With a rich premixed mixture at low strain rates and pressures, high exothermic reactions producing CO2 and H2O, and consuming CO and H2 causes a heat-release-rate peak. Unexpected character of the lean and rich premixed flames is observed, leading to the conclusion that these flames are diffusion-controlled.

Keywords: Branched flame, Strained Flame

*Corresponding author
Email address: clopezca@uci.edu (Claudia-F. López-Cámara1,*)
1. Introduction

Flamelet studies provide insights about common behaviors that can be observed in more convoluted turbulent flames. Flamelets subjected to high strain rates have been studied with findings of multi-branched flames and also merging of branches of triple flames \cite{1,2}. Triple flames are described as tri-brachial structures composed by a fuel-lean premixed flame, a fuel-rich premixed flame, and a diffusion flame derived from the unburned reactants \cite{3,4,5}. These flames are crucial in several combustion applications such as ignition and extinction processes of non-premixed systems \cite{6}.

Rajamanickam et al. numerically investigated the influence of stoichiometry on strained triple flames in counterflow configuration \cite{7}. They used a one-step chemical kinetic model with constant density and constant transport properties. Their main conclusion was that the classical tri-branchial structure might not be observed in some cases, especially at high equivalence ratio. However, that study and the majority of studies involving multi-branched flames are performed using global chemical kinetic models \cite{4,8,9,10,11}, which might not be sufficient to predict an accurate behavior of these flames. Use of unity reaction orders for triple flame studies with global kinetics are also common and result in unrealistically symmetric triple flames \cite{9,10,12}. They are also unable to predict flame-branch merging accurately.

The current study, however, considers all the possible scenarios referred to the mixture ratio of the reactants that could lead to a multi-branched flame. In particular, three cases are considered: (i) lean premixed mixture coming from one side and non-reactive mixture with fuel coming from the other side; (ii) rich premixed mixture from one side and non-reactive mixture with oxygen from the other side; and (iii) lean premixed mixture coming from one side and rich premixed mixture coming from the other side.
Therefore, this work advances further with examination of the flames that co-exist at different mixture ratios and pressures when a variable normal strain rate is applied in a transverse direction to the flame. In contrast to previous studies, the numerical simulations herein employ a detailed chemical kinetic model. The counterflow-burner configuration is used since it has features relevant to the downstream behavior of triple flames.

2. Model and analysis

2.1. Chemical kinetic model and software

Results are obtained using the opposed-flow flame module (OPPDIF) from Chemkin-Pro® software, for all studied cases of counterflow flames in axisymmetric configuration. Individual specific heats and enthalpies are calculated from temperature polynomial fits. Chemkin-Pro® offers two detailed formulations to estimate the transport properties: mixture-averaged and multicomponent. The latter is deemed superior and chosen herein. The ideal gas law is used as the equation of state. For more details on the formulation for thermo-physical and transport properties, see the Chemkin-Pro® theory manual [13].

The chemical kinetic model here is the most recent version of the San Diego Mechanism, which was last updated in 2018 to include two new reactions related to CHCHO production and consumption. The San Diego Mechanism includes a total of 270 reactions and 58 species [14].

2.2. Boundary conditions

Boundary conditions are prescribed for the species mass fractions, temperature, pressure, and inlet velocities for each nozzle (Tables 1 and 2). The distance between the two nozzles is 2 cm.

The global strain rate $S$ is calculated following the expression $S = 2 \frac{V_{\text{left}}}{L}$, where $V_{\text{left}}$ is the velocity at the left inlet nozzle, and $L$ is the distance between the two nozzles.
Table 1 – Boundary conditions.

|                | Inlet (left) | Inlet (right) | Strain \((S, [s^{-1}])\) |
|----------------|--------------|---------------|--------------------------|
| Velocities \((V, [m/s])\): 4 cases | 0.1          | 0.1           | 10                       |
|                | 0.5          | 0.5           | 50                       |
|                | 1            | 1             | 100                      |
|                | 1.5          | 1.5           | 150                      |
| Temperature \((T, [K])\) | 298          | 298           | –                        |
| Pressure \((P, [atm])\) | 1 up to 20   | 1 up to 20    | –                        |

Table 2 – Species boundary conditions. Mass fractions and equivalence ratios \((\phi)\).

|                                 | Case 1 | Case 2 | Case 3 |
|---------------------------------|--------|--------|--------|
| **Nozzle:**                     |        |        |        |
| Mixture Type:                   |        |        |        |
| Fuel Lean                       | Left   | Right  |        |
| One Reactant                    |        |        |        |
| \(\phi=0.34\)                   |        |        |        |
| Methane \((CH_4)\)              | 0.02   | 0.25   | 0.02   |
| Nitrogen \((N_2)\)              | 0.7546 | 0.75   | 0.7546 |
| Oxygen \((O_2)\)                | 0.2254 | 0.1725 | 0.2254 |

3. Results and Discussion

This section is divided in three sub-sections that correspond to each of the three studied cases according to Table 2.

The non-orthodox variable \(\xi\) is employed to separate the heat-release-rate peaks while normalizing the x-axis (Eq. 1). In Equation 1, \(s.p\) stands for *stagnation plane* and \(\chi\) is a dummy variable, used only as integration limit, and corresponding to distance measured from the left nozzle \(x\). In the plots, the stagnation plane location is marked by a green dashed vertical line and placed at zero. This should help visualize the position of the flames with respect to the stagnation plane and the mixing-layer thickness (denoted as \(MLT\) in the figures, and as \(\delta\) in Eq. 2). The range of \(\xi\) magnitudes in the horizontal axis of each
plot is unity, making them comparable visually even though their stagnation planes are shifted.

\[
\xi = \frac{\int_0^X Tdx}{\int_0^L Tdx} - \frac{\int_0^{L_p} Tdx}{\int_0^L Tdx} 
\]

\[
\delta \approx \sqrt{D_T/S} 
\]

The mixing-layer thickness is estimated using the expression in Equation 2, where the thermal diffusivity \( D_T \) is taken from the reacting mixture (Cases 1 and 2) or from the average of thermal diffusivities of both reacting mixtures (Case 3). RefProp \[15\] is employed to calculate the properties of each mixture at the different pressures of study. Doing so, the Prandtl number in all cases is determined to be between 0.7 and 0.72. The definition of \( \delta \) is arbitrary and results will show that significant mixing for both premixed and non-premixed flame structures can occur outside the indicated bounds.

For the following discussion, it is important to consider Table 3, which shows the computed adiabatic flame temperatures at stoichiometric mixture ratio, as well as for the relevant equivalence ratios for this study.

Table 3 – Adiabatic flame temperatures [K] for relevant mixtures at various pressures with initial temperature of 298 K. Equivalence ratios (\( \phi \)).

| \( P \) [atm] | Stoichiometric mixture | Case 1 | Case 2 |
|---------------|------------------------|--------|--------|
| \( \phi = 1 \) | \( \phi = 0.34 \) | \( \phi = 5.70 \) |
| 1             | 2224.54                | 1152.33| 884.9  |
| 10            | 2267.12                | 1152.33| 991.45 |
| 20            | 2276.6                 | 1152.33| 1026.86|

3.1. Case 1

A fuel-lean mixture is injected from the left nozzle while diluted fuel enters the domain from the right side. Two flames are expected a priori: one premixed
flame burning all the fuel from the left and one diffusion flame burning the leftover oxidizer from the left with the fuel from the right. Results are shown in Figure 1. Pressure and strain rate effects are described in the next two Subsections 3.1.1 and 3.1.2.

3.1.1. Pressure Effects

The heat release rate is taken as a marker of flame presence in the figures. The dominant flame, in terms of the peak value of heat release rate in Figure 1, is the premixed flame on the left rather than the diffusion flame at low pressures (upper plot). However, this relative importance switches at higher pressures for both strain rates studied.

From the same figure, comparing the different heat release rates for \( S = 10 \, \text{s}^{-1} \) and \( S = 50 \, \text{s}^{-1} \) it is seen that the two flames become more independent as pressure increases - i.e. the heat-release-rate peaks are more distinct, even though the flames are getting closer. This behavior is expected since the combustion rate is enhanced when increasing pressure and it is in agreement with recent analysis using one-step Westbrook-Dryer kinetics for propane [16].

Note that an endothermic region is found in most cases. A plausible hypothesis based on the review of that region (Figure 2) is that, under certain conditions, methane converts to methyl (CH\(_3\)), which might recombine to form ethane (C\(_2\)H\(_6\)) and then, ethane dehydrogenates to ethylene (C\(_2\)H\(_4\)). This is a highly endothermic process [17] that is only considered in detailed chemical kinetic models and explains the endothermic region found in these simulations. Similar trends and a characteristic endothermic region were observed when simulating this case using the DRM19 chemical kinetic model (84 reactions, 19 species [18]). The results shown using that model (Figure 3) at lower pressures at these strain rates qualitatively support the features that were obtained using the San Diego Mechanism.
Figure 1 – Comparison between two different strain rates for Case 1 at 1 atm, 10 atm and 20 atm. $S = 10 \text{ s}^{-1}$ (left) and $50 \text{ s}^{-1}$ (right). San Diego Mechanism. Mole fractions of $\text{CH}_4$, $\text{O}_2$ and $\text{N}_2$ (black) and heat release rate (orange). Stagnation plane location (green) and the estimated mixing-layer edge (red). See the online version for color references.

Figure 2 – Result for Case 1 with $S = 50 \text{ s}^{-1}$ at 20 atm. San Diego Mechanism. Mole fractions of $\text{CH}_3$, $\text{C}_2\text{H}_6$ and $\text{C}_2\text{H}_4$ (black). Heat release rate (orange). Stagnation plane location (green) and the estimated mixing-layer edge (red). See the online version for color references.
Figure 3 – Comparison between two different strain rates for Case 1 at 10 atm. $S = 10 \text{s}^{-1}$ (left) and $50 \text{s}^{-1}$ (right). DRM19 model. Mole fractions of CH$_4$, O$_2$ and N$_2$ (black) and heat release rate (orange). Stagnation plane location (green) and the estimated mixing-layer edge (red). See the online version for color references.

3.1.2. Strain Rate Effects

In all pressure and strain rate conditions, two flames can be observed. Both flames are placed on the left of the stagnation plane and the flame on the left becoming dominant over the diffusion flame at low pressures. Our results indicate that increasing strain rate at constant pressure favors flame merging, especially at low pressures. Therefore, lower strain rates allow easier distinction between existing flame peaks.

Analysing the character of these flames in depth, it is concluded that the flame expected to be partially premixed (left) does not follow the classical premixed characteristics - i.e. flame peak temperature is lower than adiabatic flame temperature, and velocity remains constant at constant pressure when increasing strain rate. The temperature of this flame is over the adiabatic flame temperature expected for the equivalence ratio ($\phi = 0.34$) (see Tables 3 and 4). Additionally, Figure 4 and Table 5 show that at constant pressure, the velocity at the partially-premixed flame front does not remain constant when varying the strain rate, but rather increases with it. These observations indicate that as strain rate increases, the gradients between the two flames also increase and the distance between flames decreases, leading to an increase of diffusion rates. In other words, increasing the strain rate enhances reactants mass transport towards the diffusion flame, producing more heat, which in turn is transported
Table 4 – Characteristics of the heat release rate ($Q$) peaks for Cases 1 and 2. $T$ stands for temperature.

| Case | $P$ [atm] | $S$ [s$^{-1}$] | $\xi \text{ at } Q \text{ peak}$ | Character of $Q$ peak | $T$ at peak [K] |
|------|-----------|----------------|---------------------------------|-----------------------|----------------|
| 1    | 10        | 10             | -0.586                          | Lean premixed flame with diffusive character | 1363.90 |
|      |           |                 | -0.277                          | Diffusion flame       | 1945.35 |
|      |           |                 | -0.409                          | Lean premixed flame with diffusive character | 1351.28 |
|      |           |                 | -0.209                          | Diffusion flame       | 1896.72 |
| 10   |           | 10             | -0.339                          | Lean premixed flame with diffusive character | 1525.77 |
|      |           |                 | -0.210                          | Diffusion flame       | 2100.02 |
|      |           |                 | -0.181                          | Lean premixed flame with diffusive character | 1601.63 |
|      |           |                 | -0.114                          | Diffusion flame       | 2042.00 |
| 20   |           | 10             | -0.264                          | Lean premixed flame with diffusive character | 1521.45 |
|      |           |                 | -0.162                          | Diffusion flame       | 2124.70 |
|      |           |                 | -0.135                          | Lean premixed flame with diffusive character | 1653.12 |
|      |           |                 | -0.093                          | Diffusion flame       | 2073.30 |
| 1    | 10        | 10             | -0.440                          | Rich premixed flame with diffusive character | 1576.99 |
|      |           |                 | -0.240                          | Diffusion flame       | 2010.19 |
|      |           |                 | -0.155                          | Exothermic reactions (no flame)  | 2009.53 |
|      |           |                 | 0.039                           | Rich premixed flame with diffusive character | 1726.23 |
|      |           |                 | 0.150                           | Diffusion flame       | 2040.70 |
|      |           |                 | 0.232                           | Exothermic reactions (no flame)  | 1953.67 |
| 2    | 10        | 10             | -0.310                          | Rich premixed flame with diffusive character | 1528.33 |
|      |           |                 | -0.106                          | Diffusion flame       | 2217.03 |
|      |           |                 | 0.005                           | Rich premixed flame with diffusive character | 1654.69 |
|      |           |                 | 0.107                           | Diffusion flame       | 2259.32 |
| 20   |           | 10             | -0.305                          | Rich premixed flame with diffusive character | 1168.04 |
|      |           |                 | -0.078                          | Diffusion flame       | 2253.03 |
|      |           |                 | -0.002                          | Rich premixed flame with diffusive character | 1619.59 |
|      |           |                 | 0.085                           | Diffusion flame       | 2308.72 |
at a faster rate towards the partially premixed flame. The latter also produces more heat - highlighted by its peak temperature being higher than its corresponding adiabatic flame temperature- and is able to sustain higher velocities than it would if it behaved like a typical premixed flame.

![Graphs showing comparisons](image)

**Figure 4** – Comparison between two different strain rates for Case 1 at 1 atm, 10 atm and 20 atm. \( S = 10 \text{s}^{-1} \) (left) and \( 50 \text{s}^{-1} \) (right). Velocity \( (v) \) and density \( (\rho) \) times velocity are plotted. San Diego Mechanism. Stagnation plane location (green) and the estimated mixing-layer edge (red). See the online version for color references.

### 3.2. Case 2

In this case, a fuel-rich mixture is injected from the left nozzle while air enters the domain from the right side. Here, two flames are expected: a premixed flame burning the fuel stoichiometrically from the left and a diffusion flame burning the leftover fuel from the left with the air from the right. However, due to the
Table 5 – Flame front velocities [cm/s] at different pressure ($P$) and strain rate ($S$) conditions for Cases 1 and 2.

| $P$ [atm] | $S$ [$s^{-1}$] | 10  | 50  |
|-----------|----------------|-----|-----|
|           |                |     |     |
| Case 1    |                |     |     |
| 1         | 17.0           | 33.01 |
| 10        | 4.76           | 10.16 |
| 20        | 3.18           | 7.147 |
| Case 2    |                |     |     |
| 1         | 3.98           | 9.02  |
| 10        | 1.90           | 3.89  |
| 20        | 1.69           | 3.03  |

same reasons discussed in Case 1, the partially premixed fuel-lean flame is also diffusion controlled. Its peak temperature is also higher than the corresponding adiabatic flame temperature at the in-flowing mixture ratio, and the velocity at the flame front increases with strain rate at constant pressure. Solutions for this case are portrayed in Figure 5 and more details follow in the next Subsections 3.2.1 and 3.2.2.

3.2.1. Pressure Effects

As in the previous case, Figure 5 shows that increasing pressure enhances the combustion; therefore, higher heat release rates are obtained. The diffusion flame (left heat-release-rate peak) is dominant for all pressures and strain rates.

At low pressure (1 atm) and especially at high strain rate, merged flames are observed which become distinct and branch into two co-existing flames when increasing pressure and maintaining constant strain rate. Figure 5 also shows that depending on the pressure and strain, the diffusion flame (right) possesses two local peaks in heat release rate: one at $\xi = -0.240$ and the other at $\xi = -0.155$ (1 atm and 10 s$^{-1}$), while the peak at $\xi = -0.440$ corresponds to the partially-premixed fuel-rich flame (see Table 4). There is only one peak in temperature (see Figure 6). In the local absence of methane, the heat-release-
rate peak at $\xi = -0.155$ is mostly produced by reactions $R_1$ and $R_2$ which are highly exothermic (i.e. negative reaction enthalpy $\Delta H_R$) and displaced to the formation of products. Figures 6 and 7 show that the maximum temperature and concentration of CO$_2$ and H$_2$O occur at the valley between $\xi = -0.240$ and $\xi = -0.155$. However, concentrations of CO and H$_2$ peak in the region between the partially premixed rich flame and the diffusion flame. These two species are not fully depleted across the left peak of the diffusion flame, hence enabling reactions $R_1$ and $R_2$ to be active in the right peak of the same flame. The relative importance of certain reaction pathways at the locations of the three reaction peaks is highlighted in Figure 8. Bolder lines imply a more important pathway. Thus, it is expected that the pathways that relate to the partially-premixed fuel-rich flame (Subfigure 8a left, $\xi = -0.440$) are thicker than the ones presented for the diffusion flame (Subfigure 8b left, $\xi = -0.240$) or when there is no flame (Subfigure 8c, $\xi = -0.155$). Moreover, Subfigure 8c (left and right) further supports that reactions $R_1$ and $R_2$ are the cause for the right peak of the diffusion flame, since pathways that lead to reactions $R_1$ and $R_2$ are represented by darker and thicker arrows.

\[
\begin{align*}
\text{CO} + \text{OH} & \rightleftharpoons \text{CO}_2 + \text{H} \quad \Delta H_R = -320.443 \text{ kJ mol}^{-1} \quad (R1) \\
\text{H}_2 + \text{OH} & \rightleftharpoons \text{H}_2\text{O} + \text{H} \quad \Delta H_R = -279.328 \text{ kJ mol}^{-1} \quad (R2)
\end{align*}
\]

3.2.2. Strain Rate Effects

Figure 5 shows that lowering strain rate separates the different flame branches, while increasing it at constant pressure causes merger. The effect of strain rate is better observed at low pressure (1 atm) and agrees with the observations from Sirignano [16].

Variations in strain rate have a major impact on the location and the character of the flames. In this Case 2, as in the previous case and contrary to
Figure 5 – Comparison between two different strain rates for Case 2 at 1 atm, 10 atm and 20 atm. \( S = 10 \, \text{s}^{-1} \) (left) and \( 50 \, \text{s}^{-1} \) (right). San Diego Mechanism. Mole fractions of \( \text{CH}_4 \), \( \text{O}_2 \) and \( \text{N}_2 \) (black) and heat release rate (orange). Stagnation plane location (green) and the estimated mixing-layer edge (red). See the online version for color references.

Figure 6 – Case 2 at \( S = 10 \, \text{s}^{-1} \) and 1 atm. San Diego Mechanism. Temperature (black) and heat release rate (orange). Stagnation plane location (green) and the estimated mixing-layer edge (red). See the online version for color references.

expectation, the character of the premixed flame does not follow the classical premixed flame behavior for any of the conditions studied. The temperature
Figure 7 – Case 2 at $S = 10 \text{s}^{-1}$ and 1 atm. San Diego Mechanism. Mole fractions of CO (green), CO$_2$ (blue), H$_2$ (black), and H$_2$O (magenta) and heat release rate (orange). Stagnation plane location (green) and the estimated mixing-layer edge (red). See the online version for color references.

of this flame is, again, higher than the adiabatic flame temperature expected for the equivalence ratio ($\phi$) = 5.70 (see Tables 3 and 4). Figure 9 and Table 5 also show that, similarly to Case 1, the velocity does not remain constant when varying the strain rate. Analogous examination to that for Case 1 in Subsection 3.1.2 is followed. Consequently, similar to Case 1, the partially premixed flame is diffusion controlled. This character is strengthened for the higher strain rate (50 s$^{-1}$) cases, where both flames are within the mixing-layer boundaries. For all pressures at high strain rate, the left flame falls on the stagnation plane while the right flame is placed on the right side. This implies once again that the premixed left flame has diffusion character even though it receives both reactants from a single side.

At low strain rate (10 s$^{-1}$), the purely diffusion flame (right flame) is found just where the mixing-layer “edge” is. The edge point is based only on an order-of-magnitude estimate and the flame actually lies in the mixing layer. All the remaining methane that passes through the premixed flame without burning is consumed in this flame. For all pressures at low strain rate, both flames are placed to the left side of the stagnation plane.
Figure 8 – Main reaction pathways for species containing carbon (left) and hydrogen (right) at the three locations where reaction rate has a local maximum, (a) $\xi = -0.440$ (b) $\xi = -0.240$ (c) $\xi = -0.155$. Case 2 with $S = 10 \text{s}^{-1}$ at 1 atm. San Diego Mechanism. Thickness of the arrows represent the importance of the reaction pathway.
Figure 9 – Comparison between two different strain rates for Case 2 at 1 atm, 10 atm and 20 atm. $S = 10 \text{s}^{-1}$ (left) and $50 \text{s}^{-1}$ (right). Velocity ($v$) and density ($\rho$) times velocity are plotted. San Diego Mechanism. Stagnation plane location (green) and the estimated mixing-layer edge (red). See the online version for color references.

3.3. Case 3

A fuel-lean mixture is injected from the left nozzle while a fuel-rich mixture enters the domain from the right side. Three flames are expected in this case: one premixed flame burning the fuel stoichiometrically from the right, one premixed flame burning all the fuel from the left, and one diffusion flame in the middle burning the leftover fuel and air coming from the right and left sides, respectively.

For this more complex case, two extra strain-rate values have been studied ($100 \text{s}^{-1}$ and $150 \text{s}^{-1}$) and the corresponding pressure effects can be seen in Figures 10 and 11.
3.3.1. Pressure Effects

As described for Cases 1 and 2, flames become more distinct from each other as pressure is increased. This effect can be observed for all strain rates, but it manifests best at the highest strain rate. In the cases when \( S = 100 \, \text{s}^{-1} \) and \( 150 \, \text{s}^{-1} \), only two flames are observed at low pressure, being a premixed fuel-lean diffusion character flame (left) and a diffusion flame (right). Notice that Figure 11 clearly shows that the flame on the right has a diffusive character since reactants arrive from opposite sides of the domain and get consumed where the heat-release-rate peaks. Therefore, it is concluded that the expected premixed fuel-rich flame is merged with the diffusion flame.

The character of these flames can be classified, from left to right, as fuel-lean partially premixed and diffusion controlled, diffusion, and fuel-rich having both diffusion and premixed character (see Table 6 for more details). For most configurations, the peak heat release rate is higher from left to right, with the fuel rich flame being the weakest of the three (see Figures 10 and 11). However, at the highest pressure for the lower strain rates of 10 \( \text{s}^{-1} \) and 50 \( \text{s}^{-1} \) (Figure 10), the diffusion-flame reaction peak is the highest. See Figure 12 where this is highlighted; there is a crossover at a given strain rate where the lean-premixed flame switches from weaker to stronger compared to the diffusion flame. This crossover point occurs at higher strain rate with increasing pressure. Residence time for the diffusion flame is proportional to the reciprocal of strain rate. The diffusion flame weakens with decreasing residence time since a certain time is needed for complete reaction. That being said, the integral of the heat release rate versus the axial coordinate shown in Figure 13 clearly highlights how the jump corresponding to the diffusion flame is larger than those related to the other heat-release-rate peaks. Therefore, the diffusion flame produces more heat even for the cases where the fuel-lean partially premixed flame heat-release-rate peak is higher. That is explained as follows: for the case with a mass fraction of 0.02 for the fuel to be burned in the lean flame, only an \( \text{O}_2 \) fraction of a 0.04
will be consumed there, leaving a mass fraction of about 0.185 to be consumed in the diffusion flame.

Examining the case at the lowest pressure and strain rate, the lean and rich premixed flames are represented by the heat-release-rate peaks placed at $\xi = -0.612$ and $\xi = -0.045$, respectively. The premixed flame establishes its residence time based on pressure and mixture ratio without regard to strain rate. It simply relocates its position so that its propagation velocity matches the incoming stream velocity. The heat-release-rate peak observed at $\xi = -0.340$ refers to the zone where exothermic reactions $\text{R1}$ and $\text{R2}$ are occurring. Therefore, the region from $\xi = -0.340$ to the end of the domain shows similar behavior to the one explained for Case 2 in Section 3.2.1. In this case, this heat-release-rate peak is placed at the left side of the rich premixed flame peak and on the right of the diffusion flame peak, since the rich premixed mixture comes from the left side of the domain - i.e., opposite side than in Case 2.

| $P$ [atm] | $S$ [s$^{-1}$] | $\xi$ at $Q$ peak | Character of $Q$ peak | $T$ at peak [K] |
|-----------|---------------|------------------|---------------------|----------------|
| 1         | 10            | -0.612           | Lean premixed flame with diffusive character | 1364.42        |
|           |               | -0.340           | Exothermic reactions (*no flame*) | 2067.00        |
|           |               | -0.245           | Diffusion flame      | 2051.22        |
|           |               | -0.045           | Rich premixed flame with diffusive character | 1606.51        |
| 50        | -0.436        | Lean premixed flame with diffusive character | 1380.28        |
|           |               | -0.187           | Diffusion flame      | 2007.65        |
|           |               | -0.059           | Rich premixed flame with diffusive character | 1670.89        |
| 100       | -0.389        | Lean premixed flame with diffusive character | 1350.18        |
|           |               | -0.186           | Diffusion flame      | 1979.44        |
| 150       | -0.361        | Lean premixed flame with diffusive character | 1369.71        |
|           |               | -0.192           | Diffusion flame      | 1960.90        |

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Table 6 – continued from previous page

| $P$ [atm] | $S$ [s$^{-1}$] | $\xi$ at $Q$ peak | Character of $Q$ peak | $T$ at peak [K] |
|-----------|---------------|-------------------|----------------------|----------------|
| 10        | 10            | -0.376            | Lean premixed flame with diffusive character | 1526.31 |
|           |               | -0.230            | Diffusion flame       | 2255.97 |
|           |               | 0.000             | Rich premixed flame with diffusive character | 1520.22 |
| 50        | -0.210        | Lean premixed flame with diffusive character | 1593.89 |
|           | -0.135        | Diffusion flame   | 2193.047             |
|           | -0.019        | Rich premixed flame with diffusive character | 1626.38 |
| 100       | -0.177        | Lean premixed flame with diffusive character | 1633.23 |
|           | -0.126        | Diffusion flame   | 2155.22             |
|           | -0.047        | Rich premixed flame with diffusive character | 1710.69 |
| 150       | -0.161        | Lean premixed flame with diffusive character | 1643.07 |
|           | -0.120        | Diffusion flame   | 2132.86             |
|           | -0.058        | Rich premixed flame with diffusive character | 1745.86 |
| 20        | 10            | -0.304            | Lean premixed flame with diffusive character | 1519.78 |
|           | -0.188        | Diffusion flame   | 2283.75             |
|           | 0.063         | Rich premixed flame with diffusive character | 1134.40 |
| 50        | -0.160        | Lean premixed flame with diffusive character | 1645.40 |
|           | -0.106        | Diffusion flame   | 2232.40             |
|           | -0.014        | Rich premixed flame with diffusive character | 1642.81 |
| 100       | -0.134        | Lean premixed flame with diffusive character | 1674.86 |
|           | -0.096        | Diffusion flame   | 2206.48             |
|           | -0.032        | Rich premixed flame with diffusive character | 1664.28 |
| 150       | -0.121        | Lean premixed flame with diffusive character | 1698.14 |
|           | -0.092        | Diffusion flame   | 2182.94             |
|           | -0.042        | Rich premixed flame with diffusive character | 1713.78 |
Figure 10 – Comparison between two different strain rates for Case 3 at 1 atm, 10 atm and 20 atm. $S = 10 \; s^{-1}$ (left) and 50 $s^{-1}$ (right). San Diego Mechanism. Mole fractions of CH$_4$, O$_2$ and N$_2$ (black) and heat release rate (orange). Stagnation plane location (green) and the estimated mixing-layer edge (red). See the online version for color references.

3.3.2. Strain Rate Effects

At high strain rate ($100 \; s^{-1}$ and $150 \; s^{-1}$), the heat-release-rate peak of the flames increases from right to left, with the fuel rich partially premixed flame being the weakest of the three. This is also true at low strain rates. Note that the important factor is the integral of the reaction rate through the reaction zone rather than the peak value in terms of total heat release rate. Not many general flame behavioral differences were found between the high strain rates studied. However, the peaks of the flame are getting closer and further from the stagnation point, approaching the estimated mixing-layer edge. This behavior indicates a likely flame merging at still higher strain rates.
Figure 11 – Comparison between two different strain rates for Case 3 at 1 atm, 10 atm and 20 atm. $S = 100 \text{ s}^{-1}$ (left) and $150 \text{ s}^{-1}$ (right). San Diego Mechanism. Mole fractions of CH$_4$, O$_2$ and N$_2$ (black) and heat release rate (orange). Stagnation plane location (green) and the estimated mixing-layer edge (red). See the online version for color references.

4. Conclusions

Flame merging has been observed numerically and experimentally for practical turbulent combustion situations. The novelty of the current numerical study is the in-depth analysis of the flame merging and separation processes entailing detailed chemistry and transport, and employing the counterflow canonical configuration commonly used in experimental studies. This is achieved by examining previously unreported mixture ratios in-flowing from each nozzle of the counterflow configuration.
Case 3. San Diego Mech.

**Figure 12** – Case 3. Heat-release-rate peaks for different strain rates at pressures of 1 atm (red), 10 atm (dark blue), 20 atm (green), 30 atm (light blue), 40 atm (pink). Only lean-premixed flame (triangles) and diffusion flame (circles) peaks are represented. San Diego Mechanism. See the online version for color references.

**Figure 13** – Comparison between two different strain rates for Case 3 at 10 atm and 20 atm. $S = 10\, \text{s}^{-1}$ (left) and $50\, \text{s}^{-1}$ (right). San Diego Mechanism. Stagnation plane location (green) and the estimated mixing-layer edge (red). See the online version for color references.

This study describes the important roles that normal strain rate and pres-
sure have with flames. An increase in the normal strain rate and/or a decrease in the pressure causes flames to merge while strain rate decreases and/or pressure increases lead to multiple flames.

Moreover, an endothermic region is observed for Case 1. This finding has to be further investigated. However, a preliminary explanation related to the production of ethylene (C\textsubscript{2}H\textsubscript{4}) is plausible.

At low strain rates and pressures, and only when a rich premixed mixture is injected, an extra heat-release-rate peak is obtained. After our investigation, this heat-release-rate peak is linked to high exothermic reactions producing CO\textsubscript{2} and H\textsubscript{2}O, and consuming CO and H\textsubscript{2}.

In the different multi-branched flames studied, unexpected character of the lean and rich premixed flames indicates that they are diffusion-controlled rather than possessing a classical wave-like nature strongly dependent on chemical kinetic rates.

Further research should be conducted to characterize the extinction rate for the studied cases.

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