Spin-wave amplification techniques are key to the realization of magnon-based computing concepts. We introduce a novel mechanism to amplify spin waves in magnonic nanostructures. Using the technique of rapid cooling, we create a non-equilibrium state in excess of high-energy magnons and demonstrate the stimulated amplification of an externally seeded, propagating spin wave. Using an extended kinetic model, we qualitatively show that the amplification is mediated by an effective energy flux of high energy magnons into the low energy propagating mode, driven by a non-equilibrium magnon distribution.

In recent years, the search for alternative computing methods has sparked interest in analog computing schemes that take advantage of the speed, parallelization and non-binary nature of physical systems [1–4]. Spin waves offer unique properties, such as intrinsic nonlinearity, interference, and scalability, making them an efficient carrier of information for such tasks [5–7]. A variety of spin-wave based devices have been presented, forming the building blocks for more complex magnonic systems [6–10]. However, there is a major limitation when combining these components to achieve more intricate functionalities. The spin-wave decay through relaxation mechanisms sets a natural limit to the computational complexity that can be achieved. Therefore, methods are required to efficiently and selectively amplify and sustain spin-wave signals beyond their intrinsic lifetime, enabling for the cascading of logic elements and achieving a fan-out capability.

Currently, two mechanisms are being explored for spin-wave amplification. The first method is based on the splitting of microwave photons into magnon pairs at half the microwave frequency, known as parametric amplification [11–15]. This technique has been successfully employed to amplify propagating spin waves in macroscopic [11] and microscopic [12–14] structures. While its fundamental applicability in nanoscopic systems has been demonstrated recently, parametric amplification and its efficiency in these systems is still subject of current research [16]. The second method known to amplify spin waves is based on the injection of spin-currents and the associated spin-transfer torques (STT). These currents can be generated, for instance, by using an additional magnetic ‘polarizer’ to spin-polarize a charge current [17, 18], or by taking advantage of effects such as the spin Hall effect (SHE) [19–21] or the spin Seebeck effect (SSE) [22, 23]. This method allows for partial or even overcompensation of the spin-wave damping [24]. A drawback of using the SHE for this approach is the requirement of spin injection layers, which naturally reduce the spin-wave lifetime through spin-pumping and microwave eddy currents, thereby counteracting the desired amplification.

In this study, we take a fundamentally different approach to spin-wave amplification which is based on the stimulated emission of magnons. In thermodynamic equilibrium, typically, a stimulated amplification process cannot achieve a net energy gain. Instead, analogous to the amplification in a LASER, a non-equilibrium energy distribution is required. To achieve such state, we use the method of rapid cooling [25–27]: A microscopic yttrium iron garnet (YIG) waveguide is locally heated by a short DC current pulse in an adjacent metal. When the DC pulse is turned off, the heat rapidly dissipates to the surrounding material, causing a sudden decrease in lattice temperature. This process is approximately instant compared to the magnon lifetime in YIG, causing an imbalance between the lattice and the magnon system. In the process of the reduction of the free energy of the system, the excess magnons are redistributed towards the bottom of the magnon spectrum. This process can trigger the formation of a magnon Bose-Einstein condensate (BEC) [25, 27], or stabilize a nonlinear, localized magnonic bullet mode below the bottom of the magnon spectrum [26]. We have shown that these phenomena can be understood in the simplified picture of a quasi-equilibrium approximation of the rapid cooling process using a global chemical potential $\mu$. Here, we theoretically take into account the non-equilibrium nature of the rapid cooling process by introducing a local chemical potential $\mu_k$ and local temperature $T_k$ to the kinetic model developed in Ref. [25]. We find that a net energy flow to spin-wave modes even above the minimum frequency of the magnon spectrum can occur, driven by the non-equilibrium excess of high-energy magnons. Experimentally, we investigate this process by seeding the rapidly cooled magnon gas with an externally excited, propagating spin-wave packet. This serves as an attractor state to the redistribution process, leading to stimulated amplification.

Previous approaches to spin-wave lasing have utilized electron-mediated mechanisms such as spin-wave/carrier-wave interactions [28–30], spin-transfer torques [17, 31–33] or an effect known as quantum amplification [34, 35] to pump the spin-wave system. The most crucial difference between our experiments and previous approaches is that we realize a...
thermodynamic LASER where the energy is provided by an incoherently and thermally pumped, non-equilibrium magnon distribution.

The investigated microstructure and the experimental setup are shown in Fig. 1. The structure consists of a 34-nm-thick and 2-µm-wide yttrium iron garnet (YIG) waveguide, fabricated by argon ion milling (see, for instance, Ref. [36]) from an LPE-grown YIG film [37]. Standard vector-network-analyzer ferromagnetic resonance measurements were performed on a reference pad on the sample, yielding a Gilbert damping parameter of \(\alpha = 1.8 \times 10^{-4}\). The waveguide is magnetized transversely by an external field of \(\mu_0 H_{\text{app}} = 188\) mT. A 2-µm-long area of the waveguide is covered by a pad of MgO\text{Pt} (517 nm) grown by molecular beam epitaxy, which in the following will be referred to as the amplifier pad. Electrical contacts to the amplifier pad and a stripline antenna were structured from a Ti/Au material system.

In the experiment, short DC heating pulses of length \(\tau_{\text{DC}} = 15\) ns and voltages of up to \(U_{\text{DC}} = 1.1\) V, corresponding to a current density of \(j_{\text{DC}} = (1.56 \pm 0.3) \times 10^{12}\) Am\(^{-2}\), are used to locally increase the temperature by Joule heating, see Supplemental Material [38]. The MgO interlayer serves as a spin-diffusion barrier, preventing spin injection from the Pt layer into the waveguide [39, 40]. Subsequently, after the heating pulse is turned off, a rapid cooling process takes place until a thermodynamic equilibrium is achieved. A microwave switch is used to generate a short microwave pulse (\(\tau_{\text{RF}} \approx 10\) ns) with a carrier frequency above the bottom of the spin-wave spectrum. In the following experiments, this frequency is \(f_{\text{RF}} = 7.225\) GHz, see Supplemental Material [38] for other excitation frequencies. This pulse then excites a packet of propagating spin waves in the magnonic waveguide below the RF antenna.

The resulting spin dynamics is studied with time- and space-resolved Brillouin-light-scattering (BLS) spectroscopy, using a laser beam of \(\lambda = 457\) nm and \(P = (5.0 \pm 0.5)\) mW. The employed BLS setup hosts an upside-down sample geometry, allowing to focus the laser (spot size 400 nm) from the backside of the sample through the transparent gadolinium gallium garnet (GGG) substrate onto the YIG waveguide [25–27, 36, 41]. This enables measurements in the region covered by the amplifier pad.

After the spin-wave packet is excited, it propagates along the waveguide and passes the amplifier pad. Three different pulse configurations are compared: the application of the RF pulse only, the heating pulse only, or both together. The resulting time-dependent BLS intensity, measured \(\Delta x = 1.7\) µm behind the pad, is shown in Fig. 2. For the case of only the RF pulse applied (red curve), we observe a spin-wave packet of duration \(\tau_{\text{FWHM}} = 15\) ns, to which the intensity scale is normalized. When additionally a heating pulse is sent through the amplifier pad, the result changes quite drastically. When timed such that the spin-wave packet is below the amplifier pad just when the heating pulse ends, i.e. in the moment of the largest cooling rate, the spin-wave packet is significantly amplified. The resulting BLS intensity is more than twice as high compared to the case without a heating pulse (blue curve). However, there is no spin-wave emission detected when only the heating pulse is applied. This indicates that the observed amplification is caused by an interaction between the spin-wave packet and the consequences of the heating pulse.

We quantitatively investigate this amplification as a function of the time delay \(\Delta t\) between the RF and heating pulse,
FIG. 3. Amplification factor $A$ as a function of the time delay $\Delta t$ between spin-wave packet and the DC heating pulse using a continuous representation of error bars. The delay $\Delta t$ is set to be zero for minimal transmission which marks direct pulse overlap on the amplifier pad, the shaded area marks the uncertainty regime with full or partial pulse overlap. Parameters: $\Delta t = 1.7 \mu m$, $P_{RF} = -20$ dBm.

see Fig. 3, using the amplification factor $A$, defined as $A = I_{BLS}(U_{DC})/I_{BLS}(U_{DC} = 0 V)$. As the spin-wave packet takes time to propagate through the waveguide, there is an extended window of overlap with the DC heating pulse on the amplifier pad. For the sake of simplicity, the RF pulse delay $\Delta t$ is set to be zero for minimal transmission. In the resulting graph, four different regimes can be observed.

**Regime I** The spin-wave packet passes the amplifier pad before the heating pulse is applied. As a result, no effect on the amplification factor is observed.

**Regime II** The spin-wave packet directly overlaps with the heating pulse below the amplifier pad. In this regime, it is affected by the dynamic temperature increase during the heating pulse, and the measured BLS intensity behind the pad is drastically decreased. The total overlap time is given by the length of the heating pulse and the spin-wave packet and by the time it takes the spin-wave packet to pass the amplifier pad. For $\Delta t > 0$, partial overlap with the rapid cooling process occurs, and the transition to the next regime begins.

**Regime III** In this regime, the amplification effect is observed. It is strongest when the spin-wave packet reaches the amplifier pad just after the end of the heating pulse and decreases for larger $\Delta t$ as the cooling rate decreases. Note that this window of amplification is much longer than the actual heating pulse.

**Regime IV** At the end of regime III, the amplification vanishes, and $A$ drops slightly below unity, before recovering to its value of regime I.

These results show the presence of two effects. On one hand, the direct influence of the DC heating pulse overlapping with the spin-wave packet is evident, leading to a significant decrease in spin-wave transmission in regime II. This is caused by the forced frequency downshift of the spin-wave packet on the amplifier pad during the time-dependent temperature increase induced by the DC heating pulse, and the consequent decrease in saturation magnetization $M_S$ and exchange stiffness $D_{ex}$ of YIG [42], see Supplemental Material [38]. On the other hand, there is the amplification effect, which is observed to be maximal during the rapid cooling phase in regime III, indicating that the amplification is related to the cooling rate of the system. Hence, the effect arises when the spin-wave packet propagates below the amplifier pad after the heating pulse has ended, proving that the effect is of purely thermal origin. Other effects that could be involved, such as the SHE, the SSE, or Øersted fields related to the DC heating pulse, would be maximized during direct pulse overlap and therefore can be ruled out from contributing to the amplification process. This experiment shows that the amplitude of the spin-wave signal can be controlled by a factor in a range between 0.2 (attenuation) and almost 2.5 (amplification) simply by adjusting the relative timing to the heating pulse.

The heating power scales approximately quadratically with $U_{DC}$, the influence of which is seen when comparing $U_{DC} = 1.1 V$ to $U_{DC} = 0.9 V$ in Fig. 3. The temperatures reached for $U_{DC} = 1.1 V$ are higher, leading to a more pronounced attenuation of the spin-wave packet in regime II and the cooling phase is longer as more heat needs to be dissipated, leading to an extended amplification phase III. In this phase, the formation of a second amplification plateau can be observed. This could be a product of indirect magnon redistribution processes, as it is correlated to the formation of a Bose-Einstein condensate in the region below the amplifier pad above the threshold value of $|U_{BEC}| = 1.0 V$ [25, 26].

FIG. 4. Black curve, left scale: Amplification factor $A$ as a function of the applied DC heating pulse amplitude $U_{DC}$. Measurement performed for $\Delta t = 50$ ns, $P_{RF} = -27$ dBm and in a distance of $\Delta t = 3 \mu m$ to the amplifier pad - slightly more than the previous measurements, see Supplemental Material [38] for a discussion on the impact on the amplification factor. Red curve, right scale: BLS intensity measured on the amplifier pad using only a DC heating pulse but no spin-wave excitation.
BEC formation threshold is apparent from a measurement of the BLS intensity in the amplifier pad region itself, which is shown in Fig. 4 by the red curve. Additionally, the amplification factor is shown, measured as a function of $U_{DC}$ and using a fixed delay of $\Delta t = 50\,\text{ns}$. For small amplitudes $|U_{DC}| < 0.4\,\text{V}$, the heating pulse does not affect the intensity of the spin-wave packet. For intermediate amplitudes, $0.4\,\text{V} < |U_{DC}| < 0.6\,\text{V}$, a slight attenuation is observed, which could be due to residual heat and the consequent impact on the magnetic properties of the waveguide. For amplitudes $|U_{DC}| > 0.6\,\text{V}$, the amplification process dominates, which is symmetric with respect to the sign of $U_{DC}$. This again highlights the thermal origin of the amplification effect. In contrast to the BEC formation [25], the amplification effect does not have a clear threshold value and scales with the applied heating power.

In the following, an extension of the kinetic model developed in Ref. [25] is derived for the simplified case of a thin film, which accounts for the non-equilibrium nature of the rapid cooling process. The interaction of a propagating spin-wave mode with wavevector $k$ with a rapidly cooled magnon gas can be qualitatively analyzed using the kinetic equations for the population of magnon states [43]. The influence of 4-magnon scattering leads to an additional energy flux $G_k$ for the magnon population $\tilde{n}_k$:

$$
\frac{d\tilde{n}_k}{dt} = -2(\Gamma_k + G_k)\tilde{n}_k,
$$

(1)

see Supplemental Material [38] for details. Here, $\Gamma_k$ is the spin-lattice relaxation rate. If the magnon gas is in thermodynamic equilibrium, $G_k$ can be written as

$$
G_k = \frac{1}{2} \sum_{123} T_{k123} n_1 n_2 n_3
$$

$$
\times \exp\left( \frac{\hbar \omega_1 - \mu}{k_B T} \right) \left[ \exp\left( \frac{\hbar \omega_k - \mu}{k_B T} \right) - 1 \right]
$$

(2)

where $1 \equiv k_1$, etc., where the summation includes all scattering processes satisfying energy $\omega_k + \omega_1 = \omega_2 + \omega_3$ and momentum $k + k_1 = k_2 + k_3$ conservation laws. $T_{k123} > 0$ are the 4-magnon scattering amplitudes, $n_1$ is the population of state $k_1$ in the magnon gas, and $\mu$ and $T$ are the chemical potential and temperature of the gas, respectively.

In the approximation of thermodynamic equilibrium, the chemical potential cannot exceed the gap in the magnon spectrum, meaning that $\hbar \omega_k > \mu$ and $G_k > 0$, thus the magnon-magnon interaction leads to an energy loss of the propagating spin-wave mode $\tilde{n}_k$. In the case of a non-equilibrium magnon distribution with excess of high energy magnons, however, this situation can change, as an energy flux from high energy magnon modes into the propagating spin-wave mode $k$ can arise. Here, we theoretically take into account the non-equilibrium nature of the rapid cooling process by introducing a local chemical potential $\mu_k$ and local temperature $T_k$ to the kinetic model developed in Ref. [25] and derive an equation for $G_k$ similar to Eq. (2), see Supplemental Material [38] for details. Our simulations of the population dynamics in the rapid cooling process show that, while the effective temperature $T_k$ remains almost uniform across the magnon spectrum, see Supplemental Material [38], the local chemical potential $\mu_k$ develops a significant non-uniformity.

Figure 5 shows an example dependence of $\mu_k$ on the magnon frequency $\omega_k$ for different delay times after the start of the rapid cooling process. The local chemical potential $\mu_k$ at low-energies, i.e. in the BLS observable frequency range, increases up to the magnon gap $\hbar \omega_{\text{min}}$ but never exceeds it, which is consistent with Ref. [25]. The chemical potential of higher-energy magnon states, however, significantly exceeds $\hbar \omega_{\text{min}}$ at intermediate times $t \sim 1-10\,\text{ns}$ after the onset of the rapid cooling process, which indicates the non-equilibrium character of the process. As discussed in detail in the Supplemental Material [38], this imbalance of $\mu_k$ opens new channels for an effective energy flux from a high energy mode to the propagating mode $\tilde{n}_k$, e.g. in processes such as $\omega_2 + \omega_3 \leftrightarrow \omega_1 + \omega_4$, where two degenerate magnons $\omega_2$ lead to the population of $\omega_1$ and an idler wave $\omega_4$. Respectively, the terms in Eq. (2) describing scattering with these higher-energy magnon states become negative, which can lead to the sign reversal of the magnon-magnon relaxation rate: $G_{k123} < 0$. Following Eq. (1), the high magnon population of the excited, propagating mode then acts as an attractor state to these scattered magnons.

This ‘overshoot’ of the local chemical potential $\mu_k > \hbar \omega_{\text{min}}$ at higher energy magnon states and the corresponding sign reversal of the magnon-magnon relaxation term qualitatively explains the observed amplification of propagating spin waves during the rapid cooling process. The attractive nature of the process implies that the frequency of the amplified mode is set by the incident spin-wave packet. Experimentally, the

![Graph](image_url)
frequency of the spin-wave packet is found to be preserved in the amplification process, and the amplification factor is a smooth function of the excited spin-wave frequency, see Supplemental Material [38].

In conclusion, our study has demonstrated the stimulated amplification of propagating spin waves using the technique of rapid cooling. The mechanism is based on an interaction between a propagating spin-wave mode and the rapidly cooled magnon gas. Describing the non-equilibrium population dynamics in an extended kinetic model with a local chemical potential $\mu_k$, we have qualitatively shown that this interaction results in a net energy flux driven by the scattering of excess high energy magnons. Importantly, our study has shown that the effect is achieved by a purely thermal stimulus and can be realized using spin-pumping free amplifier materials. Our results provide a proof of principle for a magnonic stimulated amplification process analogous to the LASER, pointing towards a new class of magnonic amplifiers with a potential for high efficiency and practicality.

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