Interferometry for LISA and LISA Pathfinder

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Abstract. The Laser Interferometer Space Antenna (LISA) is a joint ESA-NASA mission
designed to observe gravitational waves in the frequency range between $10^{-4}$ to 1 Hz, where
ground-based detectors are limited by terrestrial noise. Sources in this frequency range include
supermassive black holes and galactic binary stars. LISA consists of three identical spacecraft
separated by 5 million kilometers carrying a total of six free flying proof masses in heliocentric
drag-free orbit. The fluctuations in separation between two test masses located in different
satellites will be measured by laser interferometry with picometer precision. LISA Pathfinder
is a technology demonstration mission for LISA consisting of only two test masses in one single
satellite. It will be launched in 2009, five years before LISA. We provide here an overview of
the development of LISA and LISA Pathfinder with particular emphasis on the interferometry.

1. Introduction
LISA [1] will be the first gravitational wave observatory in the low frequency range, where
astrophysical events of high energy are expected. LISA is firmly established in the future
programs of both ESA and NASA, and its technology demonstrator, LISA Pathfinder, has
already entered its implementation phase.

2. LISA
The LISA constellation is shown in Figure 1. The three satellites form an equilateral triangle
that orbits the sun following the earth in a distance of 50 Million kilometer. This orbit provides a
high stability environment for the free floating test masses, so that two of them placed in different
satellites can be used as end mirrors of a high precision interferometer to detect gravitational
waves.

LISA will achieve a sensitivity to gravitational wave strain $\delta F$ in the millihertz range (Figure 2)
comparable to that of the ground base detectors at higher frequencies. Several technical
challenges have to be met to achieve this sensitivity:

Drag free control system: it must keep the residual acceleration of each test mass below
$3 \times 10^{-15} \text{ms}^{-2}/\sqrt{\text{Hz}}$ at 3 mHz.

Interferometry: its sensitivity has to be better than $40 \times 10^{-12} \text{m}/\sqrt{\text{Hz}}$ at 3 mHz.

Micronewton Thrusters: they must provide with very low noise the continuous forces of
micronewton magnitude that are necessary for the drag-free operation.

In order to test these technologies and thus mitigate risks, a Pathfinder mission will be
launched five years before LISA. Much work at the Albert Einstein Institute has been committed
to the design and implementation of the interferometry onboard this mission.
Figure 1. The three LISA satellites orbit the sun 20 degrees behind the earth in an equilateral triangle formation.

Figure 2. LISA’s dimensionless gravitational wave strain sensitivity for a signal to noise ratio (SNR) of 5 and one year integration time.

3. LISA Pathfinder
The LISA pathfinder mission (LPF) [2] consists of only one satellite (see Figure 3) carrying the European LISA Technology Package (LTP) as payload, and in addition a second set of thrusters with its drag free control system supplied by the US.

Figure 3. LISA Pathfinder satellite. The LTP is shown in the center of the satellite.

Figure 4. LISA Pathfinder will orbit the first Lagrange point.
The aim of the mission is to verify in space the LISA core technologies mentioned in section 2, mainly the drag-free control system. For its implementation, the satellite carries two free floating LISA-like test masses whose relative motion along a common sensitive axis is measured by means of a laser interferometer (see Figure 5). The position and orientation of each test mass with respect to the satellite is additionally measured by a set of electrodes that surround it. The eighteen degrees of freedom of the satellite and the two test masses are separated into "drag-free" coordinates, which are actuated by the micronewton thrusters, and the "suspension coordinates" for which the capacitive electrodes are used as actuators [2].

3.1. LISA pathfinder interferometry
A set of four non-polarizing heterodyne Mach-Zehnder interferometers will be used onboard LISA Pathfinder to detect position fluctuations of the test masses. Figure 7 illustrates their principle of function [3, 4, 5]: the laser is split into two different beams and each of them is frequency shifted by an acousto-optical modulator (AOM). The two RF frequencies that drive the AOMs differ by a constant amount of about 1 kHz, the heterodyne frequency \( f_{het} \). These two frequency shifted beams are then coupled into optical fibers and brought onto an optical bench which is made out of Zerodur for high thermal stability [6]. On the bench, the incoming beams are again split and finally brought to interference in at least two different beamsplitters (Reference and one or more Measurement).

Figure 5. LPF core assembly. Two vertical Zerodur plates hold the optical bench and the two vacuum tanks containing the test masses. Laser light from the optical bench is reflected on the test masses allowing the interferometrical determination of their position fluctuations.

Figure 6. Engineering model of the optical bench. The test masses have been substituted by gold-coated mirrors for ground testing.

On the actual LTP optical bench (Figure 8) the arms of the reference interferometer recombine directly in a beamsplitter while one of the beams of the measurement interferometer is reflected from both test mass before recombining. In addition, there are two more interferometers that are used to monitor the second test mass independently and to stabilize the laser frequency, respectively [3, 4, 7].

The heterodyne signal detected by a photodiode at the output port of each interferometer is given by:

\[
I(t) = A(1 - c \cos(2\pi f_{het} + \varphi(t)))
\]

(1)

where \( I \) is the measured intensity, \( A \) the average photocurrent of the heterodyne signal and \( c \) the interferometric contrast. The phase \( \varphi \) of the Reference and Measurement signals (Figure 7)
can be written as:

\[ \varphi_R = \frac{2\pi}{\lambda}(L_1 - L_2 + L_{1R} - L_{2R}) = \Delta_F + \Delta_R \]  
\[ \varphi_M = \frac{2\pi}{\lambda}(L_1 - L_2 + L_{1M} - L_{2M}) = \Delta_F + \Delta_M \]

where \( \Delta_F \) represents the (large) common-mode pathlength variations present in both interferometers, and \( \Delta_R \) and \( \Delta_M \) the pathlength variations on the stable optical bench of the Reference and Measurement interferometer, respectively. The main interferometrical measurement of LTP consists of a measurement of the photocurrent phase in a multichannel electronic phasemeter, and the subsequent substraction between \( \varphi_R \) and \( \varphi_M \), as this cancels the common fluctuations \( \Delta_F \) and only the position fluctuations of the test mass remain [8, 9].

**Figure 7.** Simplified schema of the interferometry concept for the LISA technology package. Only one measurement interferometer shown.

**Figure 8.** Actual layout of the ultra-stable LTP optical bench.

**Figure 9.** Sensitivity of the LTP interferometer and phasemeter for longitudinal test mass displacement.
Measurements on the engineering model of the optical bench (see Figure 6) have been done to demonstrate the sensitivity level shown in Figure 9, where the noise specification allocated for the determination of the phase difference was met. Furthermore, the use of quadrant photodiodes (QPD) allows the determination of tilt and rotations of the test masses by means of the technique "Differential Wavefront Sensing". Figure 10 shows the noise curves corresponding to these angle determination, which also fulfill the requirements.

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