Coupled-channels description of the $^{40}\text{Ca}+^{58,64}\text{Ni}$ transfer and fusion reactions

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Abstract

Preliminary experimental data for nucleon transfer reactions of the $^{40}\text{Ca}+^{58}\text{Ni}$ and $^{40}\text{Ca}+^{64}\text{Ni}$ systems are analyzed with the coupled-channels approach. It is shown that a simple treatment for the transfer in the coupled-channels method cannot reproduce simultaneously the transfer probabilities and the sub-barrier enhancement of fusion cross sections.

An extra enhancement of fusion cross sections at low energies is often attributed to different transfer processes. Several approaches have been employed in order to reproduce this enhancement. In our previous analysis [1], we attempted to reproduce simultaneously the experimental transfer probabilities and the fusion cross sections for the reaction $^{96}\text{Zr}+^{40}\text{Ca}$ [2]. The strategy was to adjust the transfer coupling to the experimental transfer data and to compare the fusion cross sections obtained with this approach to the experimental data. A slight underestimation of the fusion cross sections was found at low energies. On the other hand, Esbensen et al. [3] showed that it was possible to reproduce perfectly the fusion cross sections if one takes into account in addition the proton transfer channels.

In this contribution, we test this approach on the $^{40}\text{Ca}+^{58}\text{Ni}$ and $^{40}\text{Ca}+^{64}\text{Ni}$ systems, for which the fusion cross sections have been measured.
in ref. [4]. The TDHF theory [5] has shown that the major difference between these two systems is due to the neutron transfer. It is expected that the transfer probability for the $^{40}\text{Ca}+^{64}\text{Ni}$ system is by about one order of magnitude higher than that for the $^{40}\text{Ca}+^{58}\text{Ni}$ system. In the present contribution, we shall try to reproduce the neutron and proton transfer channels simultaneously with the enhancement of the fusion cross sections at low energies.

The experiment has been recently performed at LNL in inverse kinematics at energies around and below the Coulomb barrier. $^{64}\text{Ni}$ and $^{58}\text{Ni}$ beams were delivered by the XTU Tandem accelerator ($E_{\text{lab}}=174, 190$ and $210 \text{ MeV}$ for $^{64}\text{Ni}$, and $E_{\text{lab}}=170$ and $201 \text{ MeV}$ for $^{58}\text{Ni}$) onto a 100 micro g/cm$^2$ strip $^{40}\text{Ca}$ target deposited on a 15 micro g/cm$^2$ $^{12}\text{C}$ backing. The $^{40}\text{Ca}$ target-like ions were detected and identified by the large acceptance ($\pm 5^\circ$) PRISMA magnetic spectrometer around $\theta_{\text{lab}} = 45^\circ$. Four transfer channels were identified: +1n, +2n, -1p and -2p, where the + sign means a transfer from the Ni fragment to the $^{40}\text{Ca}$ one.

The coupled-channels calculations have been carried out with the program CCFULL [6], that has been modified in order to compute the neutron and proton transfer probabilities.

Table 1: The values of Woods-Saxon real and imaginary potentials employed in the coupled-channels calculations.

| System         | $V_0$ [MeV] | $r_0$ [fm] | $a$ [fm] | $W_0$ [MeV] | $r_W$ [fm] | $a_W$ [fm] |
|----------------|-------------|------------|----------|-------------|------------|------------|
| $^{40}\text{Ca}+^{58}\text{Ni}$ | 60.41       | 1.17       | 0.66     | 35          | 1.1        | 0.2        |
| $^{40}\text{Ca}+^{64}\text{Ni}$ | 68.70       | 1.16       | 0.66     | 35          | 1.1        | 0.2        |

The same method as in ref. [1] has been used, with values for the nucleus-nucleus potential given in tab. [1] and with the coupling parameters to the transfer channel in tab. [2]. This model assumes that the pair transfer is a sum of two processes, that is, a direct pair transfer and a sequential transfer. The sequential transfer coupling is assumed to be equal to the single transfer, i.e. $a_{12} = a_{01}$. As in ref. [4], we take into account the excitation to the first $3^-$ state in $^{40}\text{Ca}$ at energy 3.736 MeV with a coupling strength of $\beta = 0.4$, the $2^+$ state in $^{58}\text{Ni}$ at 1.454 MeV with $\beta = 0.18$, and the $2^+$ state in $^{58}\text{Ni}$ at 1.346 MeV with $\beta = 0.16$.

The transfer probabilities are computed as the ratio of the transfer cross sections to the elastic plus inelastic cross sections. The coupling parameters have been adjusted in order to reproduce the experimental transfer results as shown on the left part of figs. [1] and [2]. In these figures, the transfer
Table 2: Coupling constants for the transfer channels in the coupled-channels calculations. The parameters \(a\) are given in fm, \(\beta\) in MeV.fm and \(Q\) in MeV.

| System          | n,p | \(a\)  | \(\beta\) | \(Q\)  | \(a\)  | \(\beta\) | \(Q\)  |
|-----------------|-----|--------|----------|-------|--------|----------|-------|
| \(^{40}\text{Ca}^{58}\text{Ni}\)  | n   | 1.96   | -6       | -3.85 | 1.06   | -3       | -2.62 |
| \(^{40}\text{Ca}^{58}\text{Ni}\)  | p   | 1.96   | -16      | -4.909| 1.06   | -12      | -6.19 |
| \(^{40}\text{Ca}^{64}\text{Ni}\)  | n   | 1.16   | -37      | -1.29 | 1.06   | -27.39   | 0     |
| \(^{40}\text{Ca}^{64}\text{Ni}\)  | p   | 1.16   | -30      | -0.874| 1.06   | -20.39   | 0     |

probabilities are shown as a function of the distance of closest approach \(D\) based on the Rutherford trajectory. As expected from the \(Q\)-value, the transfer probabilities are by one order of magnitude less for the \(^{40}\text{Ca}^{58}\text{Ni}\) system than for the \(^{40}\text{Ca}^{64}\text{Ni}\) system. In the former system, the coupled-channels reproduces well the fusion cross sections because the transfer effect is too small to enhance the fusion cross sections.

Figure 1: Left: The transfer probabilities obtained experimentally (marker) and with the coupled-channels method (lines) for the \(^{40}\text{Ca}^{58}\text{Ni}\) reaction. Right: Corresponding fusion cross sections obtained experimentally and with the coupled-channels method with and without taking into account the couplings to the transfer channels (lines).

For the \(^{40}\text{Ca}^{64}\text{Ni}\) fusion reaction, the coupled-channels method predicts a small effect of the transfer. In contrast, experimentally the fusion cross sections are enhanced at energies below the barrier. Note that we can also invert the procedure, that is, by fitting the transfer coupling in order to reproduce the fusion cross sections and then comparing the transfer probabilities to the experimental data. In that case, the fusion cross sections will be well reproduced but the predicted transfer probabilities would be overestimated by about a factor of 10. In either way, it does not seem possible
with this approach to reproduce simultaneously the transfer probabilities and the sub-barrier enhancement of fusion cross sections.

In conclusion, this analysis has shown a possible limitation of the present coupled-channels method. One possibility is the coupling scheme used in refs. [1, 3, 7], that assumes that couplings to collective states are identical before and after the transfer. That is, the collective excitations and the transfer channels are treated as independent degrees of freedom. More complex models may be necessary in order to reproduce the enhancement of fusion cross sections with the coupling strengths which reproduce the experimental transfer probabilities.

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