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**Optimal Operation and Stabilising Control of the Concentric Heat-Integrated Distillation Column**

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**Abstract:** A systematic control structure design method is applied on the concentric heat-integrated distillation column (HIDiC) separating benzene and toluene. A degrees of freedom analysis is provided for identifying potential manipulated and controlled variables. Optimal operation is mapped and active constraints are identified for constructing the supervisory control layer. The fundamental problem of obtaining a stabilising control structure is addressed resulting in the regulatory control layer design. A supervisory control layer is devised and combined with the regulatory control layer. The control structure is finally evaluated by dynamic simulation for proving an acceptable performance.

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**Keywords:** Distillation columns, dynamic simulation, pressure control, heat integration, heat-pump, optimal operation

1. **INTRODUCTION**

In the heat-integrated distillation column (HIDiC), gradual condensation occurs along the rectifying section and gradual boil-up occurs along the stripping section as heat is exchanged between the sections. This can be realised by operating the rectifying section at a higher pressure by introducing a compression step above the feed stage. One proposal for realisation of the HIDiC arrangement is a concentric HIDiC (Govind, 1987), in which the high-pressure rectifying section is placed within the column shell constituting the low-pressure stripping section (see Figure 1). Each tray are heat-integrated in the same vertical position (e.g. #2 and #33) such that heat is transferred from the inner rectifying section to the outer stripping section. Due to the gradual condensation and boil-up, the column sections change cross sectional areas along their heights as indicated in the figure.

The HIDiC is a result of process intensification (PI) of a conventional distillation column by combining two phenomena (heat and mass transfer) in the column itself. The general operation implications from PI are (Nikačević et al., 2012) (i) increased operational complexity because of stronger interaction between inputs, (ii) fewer degrees of freedom, (iii) increased sensitivity to disturbances, and (iv) narrower operating windows. Some of the more established distillation column configurations, on which PI has been applied, are the dividing-wall column (DWC) and the reactive distillation column (RDC). In the DWC, more degrees of freedom (DOFs) arise while strong input-output interactions result, which leads to oscillating closed-loop responses for decentralised control (Hernández and Chinea-Herranz, 2012). The same might apply to the HIDiC due to its highly interactive nature.

Many authors consider only dual composition control schemes with dynamic HIDiC models that assume constant pressures (Nakaiwa et al., 2003; Liu and Qian, 2000; Huang et al., 2007). Only few authors consider pressure dynamics for control (e.g. Ho et al. (2009)), despite the large degree of interaction between the column pressures and the separation performance in the HIDiC. This paper addresses the design of a decentralised control structure, using a systematic approach (Skogestad, 2004) on the separation of benzene/toluene by distillation. In the process of designing the control structure, optimal and stable operation is analysed.

2. **TOOLS AND METHODS**

2.1 **Distillation Column Model**

A first-principle model of a HIDiC based on the work of Bisgaard et al. (2015) is implemented in MATLAB for simulation. The model consists of dynamic mass and energy balances, and takes into account temperature dependency of physical properties, tray pressure drops, time-varying tray pressures, and liquid and vapour hydraulics. In the following sections, relevant parts of the model are outlined, since these determines the dynamic performance of the concentric HIDiC.
of the column internals.

\[ \rho_i = \text{constant depending on the vapour loading of the individual trays [m}^2] \]

Internal Heat Integration. The internal heat transfer rate is given by

\[ q_s = UA(T_r - T_a) \]

\[ q_r = -q_s \]

where

\[ U = \text{overall heat transfer coefficient [kW m}^{-2} \text{ K}^{-1}] \]
\[ A = \text{heat transfer area (assumed constant on every tray) [m}^2] \]
\[ T = \text{temperature of a tray in the rectifying section (r) or the stripping section (s) [K]} \]

Applying Eq. (5) on the concentric HIDiC (Figure 1) gives

\[ q_{33} = UA(T_2 - T_{33}) \]

and \[ q_2 = -q_{33} \] and so on.

2.2 Control Structure Design Procedure

The control structure design procedure is outlined by Lars-son and Skogestad (2000) and Skogestad (2004) and rules for this method are collected by Minasidis et al. (2015). The procedure deals with the structural decisions that are required for the controller design. This includes the selection of manipulated variables (MVs), the selection of controlled variables (CVs), the selection of measurements for control, and the selection of their interconnection, which is termed the control configuration. The procedure consists of systematic steps, which will be applied on the concentric HIDiC. The procedure can be divided into two major steps: The top-down analysis (steady state considerations) and bottom-up (dynamic considerations).

3. SEPARATION OF BENZENE/TOLUENE

3.1 System Description

Consider the separation of 83.3 mol s\(^{-1}\) of an equimolar, saturated liquid mixture of benzene/toluene by distillation. It is desired to obtain benzene (in distillate) and toluene (in bottoms) with purities of minimum 99%. A HIDiC design with 30 trays in both sections and all being heat-integrated in the same vertical height as illustrated in Figure 1. A heat exchange area of 15 m\(^2\) per heat-integrated pair is used, which is assumed to be achieved by installing heat transfer panels (de Rijke, 2007). A conservative overall heat transfer coefficient of 0.60 kW m\(^{-2}\) K\(^{-1}\) is employed, giving \(UA = 9.0 \text{ k}W \text{ K}^{-1}\) in Eq. (5). Conventional column sizing has been employed, leading to a gradually increasing cross sectional area in the rectifying section from the top, while the stripping section cross sectional area is gradually decreasing. The combined cross sectional area (i.e. the outer column diameter) is constant. As a result, the nominal tray liquid holdups vary along the column as illustrated in Figure 2. This liquid holdup profile strongly deviate from conventional distillation columns, in which the holdup usually is approximately constant. The column dimensional parameters are provided in Table 1, while the physical parameters are accessible in the DIPPR database (AIChE, 2014). The constants \(C^L_i\) and \(C^V_i\) are calculated based on the nominal steady state liquid and

\[ V_i = C^L_i (\rho_i)^{0.5} (P_i - P_{i-1})^{0.5}/MW_i \]

Note that both \(A_{a,i}\) and \(H_{i}\) are dimensional parameters of the column internals. \(C^L_i\) is calculated from Eq. (1) from the steady state liquid flow profile.

The vapour flow through perforated plates can be described as done by Kolodzie and van Winkle (1957). In this work, the volumetric flow rate is simplified to be proportional to the square root of the pressure gradient:

\[ V_i = C^V_i (\rho_i)^{0.5} (P_i - P_{i-1})^{0.5}/MW_i \]
Fig. 2. Nominal tray holdup profile.

Table 1. Model parameters.

| Parameter                        | Value   |
|----------------------------------|---------|
| Tray pressure drop*              | 0.0070 bar |
| Liquid height over weir*         | 12.5 mm |
| Tray type                        | Sieve   |
| Weir height                      | 50 mm   |
| Internal heat transfer area per tray | 15 m²  |
| Downcomer area per tray area     | 0.07    |
| Liquid holdup time in condenser and reboiler | 300 s  |

*Used for estimating constants $C_i^L$ and $C_i^V$ in Eq. (1) and (4).

vapour flow rate profiles, the specified tray pressure drops, and the liquid heights over the weirs (Table 1). Ideal liquid and vapour phases are assumed for the vapour-liquid equilibrium relations. In addition to the concentric HIDIc, a conventional distillation column (CDiC) with the same specifications and parameters is considered in order to compare the optimal performance of the HIDIc.

3.2 Top-down Analysis

Degrees of Freedom Analysis. The operational degrees of freedom (actuators) are illustrated in Figure 1 with feed flow rate given. Seven steady state degrees of freedom correspond to the seven operational degrees of freedom. From the seven steady state degrees of freedom, the three holdups $M_{cnd}$, $M_{str}$, and $M_{rst}$ have no impact on the steady state operation (and on the cost function). Thus, four variables are available for optimisation.

Definition of Optimal Operation. Assuming an electricity price of 0.14 $\text{kHz}^{-1}$, a pressure dependent steam price starting at $22.39 \cdot 10^{-3}$ $\text{kg}^{-1}$ for 2 bar steam, a cooling water price of $0.080 \cdot 10^{-3} \text{ kg}^{-1}$, a distillate (distillate) price of 1.04 $\text{ kg}^{-1}$ ICIS (2015), a bottoms (toluene) price of 0.853 $\text{ kg}^{-1}$ ICIS (2015), and a feed price of 0.50 $\text{ kg}^{-1}$, the objective function ($J$) becomes

$$J = \min \left[ 0.50m_F - 1.04m_D - 0.853m_B \right]$$

$$+ \left( 1.99 + 20.4(P_{\text{steam}} - 1.01325)^{0.05} \right) m_{\text{steam}}$$

$$+ 0.080 \cdot 10^{-3} m_{\text{cw}} + 3.89 \cdot 10^{-5} E \right] / m_F \quad (6)$$

s.t. $0.99 \leq x_D$

$0.99 \leq 1 - x_B$

$E \leq 5000\text{kW}$

$1.013 \text{bar} \leq P_i \leq 6.0 \text{bar}$

$0.01F_0 \leq L_i \leq 200 \text{ mol s}^{-1}$

$0.01F_0 \leq V_i \leq 150 \text{ mol s}^{-1}$

where

$$J = \text{net cost per feed flow rate} \left( \frac{\text{ kg}^{-1}}{\text{ s}} \right)$$

$m = \text{mass flow rate} \left( \frac{\text{ kg}}{\text{s}} \right)$

$P_{\text{steam}} = \text{steam pressure (minimum 2 bar)} \left( \frac{\text{bar}}{} \right)$

The four optimisation DOFs are $L_{\text{cnd}}, Q_{\text{str}}, P_{\text{str}}$, and $P_{\text{rct}}$. The expected disturbance range in terms of nominal values are for the feed flow rate $0.8F_0 \leq F \leq 1.4F_0$ and benzene feed composition $0.8z_0 \leq z \leq 1.2z_0$.

Optimal Operation (Active Constraints). The solver "fmincon" in MATLAB is used for the optimisation using the sequential quadratic programming algorithm. The solution to the optimisation problem (Eq. (6)) is listed in Table 2. For comparison, the optimal operating point of a conventional distillation column (CDIC) is presented. The cost function is lower for the HIDIc, which illustrates its capability of reducing the operating cost by employing internal heat integration. Furthermore, negative objective functions are obtained, which means that profits are achieved. The nominal solution of the HIDIc has three active constraints involving $x_D$, $P_{\text{str}}$, and $L_{\text{cnd}}$ as indicated with boldface numbers (Table 2). Hence, (free DOFs)=4-3=1. In this case, one variable for self-optimising control can be used, since the active constraints must be controlled for optimum economic performance. The loss, of maintaining the bottom composition ($x_D$) or the compression ratio (CR) constant, are evaluated. It is found that $x_B$ should be used as the remaining primary controlled variable since the economic loss is the least when keeping $x_B$ constant. Thus, the primary controlled variables ($CV_1$) are $u_{\text{CV}} = [P_{\text{str}}, x_D, x_B, L_{\text{cnd}}]$. This result shows that the reflux flow rate ($L_{\text{cnd}}$) must be kept at its minimum and can, thus, not be used for temperature or composition control in the rectifying section, which typically is the case in conventional distillation. The minimum value of $L_{\text{cnd}}$ is chosen as a safety (back-off) value such that the upper trays do not dry out.

Optimal Operation. The active constraint regions are identified by the brute-force method for various disturbances. A grid of 30 nodes is used to represent the disturbance space. For each node, an optimisation is carried out and the obtained active constraint regions and objective function contours are illustrated in Figure 3.
rate \((B \rightarrow M_{rbl})\). Steady state relative gain array (RGA) (Bristol, 1966) is used to pair the remaining secondary controlled and manipulated variables. Steady state was ensured after 10 hours when imposed to a +1\% step changes in the individual input:

\[
G(s = 0) = \begin{bmatrix}
\Delta P_{rct} & \Delta P_{rct} & \Delta(\Delta T) \\
\Delta Q_{cnd} & \Delta Q_{cnd} & \Delta(\Delta T) \\
\Delta P_{cnd} & \Delta P_{cnd} & \Delta(\Delta T) \\
\Delta P_{str} & \Delta P_{str} & \Delta(\Delta T)
\end{bmatrix}
\]

\[
= 10^{-3} \begin{bmatrix}
7.2653 & 2.1645 & -63.4868 \\
3.8781 & 1.9449 & 7.4990 \\
5.2909 & 0.8490 & 2.2554
\end{bmatrix} \Rightarrow (8)
\]

Pairing on negative steady state RGA-elements is undesirable, while RGA elements of unity are preferred. Thus, it is clear that the pairing should be \((E \rightarrow P_{rct})\), \((Q_{cnd} \rightarrow \Delta T)\) and \((Q_{bl} \rightarrow P_{str})\). With this pairing, RGA elements close to unity are obtained (indicated in boldface numbers in Eq. (8)). Control of the stripping section pressure by the reboiler duty can be realised as follows: When the reboiler duty is reduced below the nominal value by the means of the controller, the net vapour flow rate through the stripping section is reduced due to the fact that the compressor dictates the flow rate of the outlet vapour.

### Design of the Supervisory Control Layer

The supervisory layer may use the setpoints to the regulatory layer as degrees of freedom to control the primary (economic) variables. As for the regulatory control layer, single-loop controllers are used for the supervisory control layer, leading to cascade controllers. The primary controlled variables were identified previously. The setpoint of the temperature profile \((\Delta T)\) is used to control the distillate composition \((x_D)\), since the distillate contains the more valuable component. Due to the close relation between the section pressures and the product compositions, the stripping section pressure setpoint is used to control the bottom composition \((x_B)\). As the stripping section pressure is a primary controlled variable, an additional control loop is added that controls the setpoint of the stripping section pressure to the optimal value. The final resulting control structure is illustrated in Figure 4.

### Controller Tuning and Evaluation

The SIMC tuning (Skogestad, 2003) is adopted for the tuning of the controllers. Only PI-controllers were used in this study. However, some rather complex open-loop responses are observed in the responses of the full-order model (Figure 5), making the tuning of the controllers a challenging task if oscillations are to be avoided. The tuning is carried out sequentially for the loops using the desired closed-loop time constant \((\tau_c)\) as the tuning parameter. The tuning sequence is based on the expectation/selection of \(\tau_c\) such that the fast loops are tuned and closed first. However, the two liquid holdup control loops were closed first \((L_{int} \rightarrow M_{rct})\) is assumed ideally controlled. Based on insights in the conventional distillation column dynamics, the tuning sequence was derived for the control structure illustrated in Figure 4. The following sequence was used after the liquid holdup loops were closed: \((Q_{bl} \rightarrow P_{str})\), \((Q_{cnd} \rightarrow \Delta T)\), \((E \rightarrow P_{rct})\), \((\Delta T_{rct} \rightarrow x_D)\), \((P_{str} \rightarrow x_B)\),

![Figure 3. Active constraint regions: I: \(x_D, P_{min}, L_{min}\), II: \(x_D, x_B, P_{min}, L_{min}\), III: \(x_D, x_B, V_{max}, E_{max}\), IV: \(x_D, x_B, V_{max}, E_{max}\), V: \(x_D, x_B, L_{max}, E_{max}\).](image-url)
The control structure is evaluated under various disturbance scenarios of which one is illustrated in Figure 6. The illustrated disturbance scenario contains both regulatory and servo responses:
\[
\begin{align*}
t &\geq 0 \text{ h: } +20\% \, F \\
t &\geq 2.5 \text{ h: } +10\% \, z \\
t &\geq 5 \text{ h: } L_{\text{cnd}}^{\text{set}} = 1.6667 \text{ mol s}^{-1} \\
t &\geq 7.5 \text{ h: } x_{D}^{\text{set}} = 0.985 \\
t &\geq 12.5 \text{ h: } x_{B}^{\text{set}} = 0.01
\end{align*}
\]
All controlled variables are kept close to their setpoints in the simulation (Figure 6). In particular, the secondary controlled variables (\(\Delta T\) and \(P_{\text{sstr}}\)) are following the setpoint trajectories, dictated by the supervisory control layer. As expected, the distillate composition is more tightly controlled than the bottoms composition, since the temperature control loop is located in the same column section of the distillate. In addition, input saturation is observed, and thus, anti-windup is included in the simulation.

4. CONCLUSION

Based on rigorous distillation column simulations of the concentric heat-integrated distillation column (HIDiC) separating a binary mixture of benzene/toluene, the following main conclusions can be extracted:

Fig. 4. Control structures for a HIDiC separating benzene/toluene. Red lines represent the regulatory control loops and blue lines represent the supervisory control loops (cascade).

and (\(P_{\text{rct}}^{\text{set}} \rightarrow P_{\text{sstr}}^{\text{set}}\)). Complex dynamic phenomena are observed, including negative and positive zeros, where the latter leads to inverse responses (Figure 5, loop \(P_{\text{sstr}}^{\text{set}} \rightarrow x_{B}\)). These responses are used to identify process transfer functions. The process transfer functions were reduced to first-order transfer functions using Skogestad’s ”half rule” (Skogestad, 2003). Furthermore, the numerator time constants (if any) were converted into time delays. Model mismatch of the low-order transfer functions are obtained due to the non-linearity of the system. The tuning parameters (\(\tau_{c}\)) for the controllers in the regulatory control layer are chosen such that fast control actions are obtained. However, it is undesirable to have fast control action of the compressor, why this is chosen as 60 seconds. The tuning parameters of the controllers in the supervisory control layer are chosen such that loop interactions are avoided. In particular, \(\tau_{c}\) of the master control loops (in the case of cascade) were chosen minimum ten times the values of the corresponding slave control loops. The tank holdups act as pure integrators and were allowed to be controlled relatively sluggishly (\(\tau_{c} = 120s\)). The values of \(\tau_{c}\) for the remaining control loops are listed in Figure 5.

The control structure is evaluated under various disturbance scenarios of which one is illustrated in Figure 6. The
Fig. 6. Selected responses of CVs and MVs to the five step disturbances. $Q_{\text{cnd}, \text{max}} = -Q_{\text{rbl}, \text{max}} = -2000$ kW and $E_{\text{max}} = 500$ kW.

i. A control structure consisting of a regulatory and a supervisory layer has been systematically derived and evaluated for a separation with a more valuable distillate product, resulting in an acceptable performance.

ii. Deriving a stabilising control system is challenging. However, in simulation we found that it can be operated steadily under realistic disturbance scenarios.

iii. There are significant interactions in both the regulatory and the supervisory layer control loops, thereby encouraging the use of e.g. multi-variable pressure control.

iv. The overall dynamics are complex giving evidence of non-linear behaviours.

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