Irradiation-induced damage in concrete-forming aggregates: revisiting literature data through micromechanics

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Abstract The radiation-induced volumetric expansion (RIVE) of aggregate-forming minerals causes damage in concrete exposed to high levels of fast neutrons fluence ($> \sim 10^{19}$ n cm$^{-2}$ at kinetics energy above 0.1 MeV). Historical post-irradiation RIVE and Young’s modulus data obtained in test reactors were revisited using a polycrystalline homogenization model (self-consistent scheme) accounting for the aggregates’ minerals content and the formation of voids/cracks during irradiation. It was found that the formation of extra voids/cracks can contribute to the aggregate expansion more substantially than the cumulated expansions of aggregate-forming minerals. The rate of void creation appears to be inversely correlated to the silica content, although aggregates of higher silicate contents exhibit higher RIVEs. The loss of Young’s modulus decreases exponentially with the aggregates’ expansion. At a comparable RIVE level, the relative loss of modulus is more significant in aggregates of higher silica content.

Keywords Radiation-induced volumetric expansion · Irradiated concrete · Polycrystalline model · Rock-forming minerals properties

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Notations The neutron fluence characterizing the number of particles crossing a unit’s surface is generally given in n cm$^{-2}$. Since irradiation exposure in light water reactors and test reactors of concrete constituents reach fluence levels of $\approx 10^{19}$–$10^{20}$ n cm$^{-2}$, fluences are alternatively given in n pm$^{-2}$. In this article, 1.0 n pm$^{-2} = 10^{20}$ n cm$^{-2}$. Also, it is convenient to express fluence for a given energy threshold, or the neutron kinetic energy. In this article, both the usual notation and a specific compact notation are used: $1.0$ n pm$^{-2}$$(E > 10$ keV) is equivalent to $1.0$ n$^{E > 10$ keV}$ pm$^{-2}$

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1 Introduction

The prospect of extending operation of nuclear power plants beyond 60 years raises critical questions about the structural integrity of the concrete biological shield against prolonged neutron and gamma irradiation. Experimental evidence shows that the primary damage mechanism of irradiated concrete is caused by the radiation-induced volumetric expansion (RIVE) of the concrete aggregates [1–5]. Meso-scale analytical [6, 7] and numerical [8, 9] models were successfully applied to derive concrete RIVE in the past. However, these models require the irradiated properties of the aggregates as inputs, which dramatically vary with the nature and composition of the rocks [1, 4].

The high-energy ballistic collisions caused by neutrons, ions, or alpha-induced recoil irradiation lead to the formation of damage cascades in rock-forming minerals’ crystalline structures, causing change of coordination of the silicate tetrahedrons. This leads to atomic bonds stretching and eventually breaking [10, 11]. Cumulated defects result in macroscopic change of the physical [4, 12–14], chemical [15–17], and mechanical properties of irradiated minerals [18–20]. Most silicate-bearing minerals, metal-bearing oxides, and to a lesser extent, carbonated minerals of initial pristine crystalline structures experience RIVE as a density decrease caused by irradiation-induced amorphization, which is also called metamictization [21]. Amorphous glassy minerals such as obsidian or vitreous silica appear to undergo moderate irradiation-induced shrinkage [18, 22]. At a given irradiation exposure, silicate-bearing minerals are subject to varied expansion levels [22]. The maximum observed RIVE value is 17.8% for fully amorphized quartz, whereas feldspars exhibit a maximum RIVE of about 7–8% and carbonates, of less than ≈1% [22, 23]. Consequently, as rocks are complex assemblages of multiple minerals of varied shapes and sizes, they also experience change in physical properties: dimensional change, general expansion, [1, 2], thermal diffusivity [1], loss of mechanical properties such as Young’s modulus [1, 2], tensile strength [1], and compression strength [4]. In some cases [4], these changes are accompanied by a modification of the stress-strain curve (gradual hardening) which origin remains to be determined. The relationship between the nature and composition of the irradiated rocks and the change of density and mechanical properties remains to be established. This relationship is critical to the assessment of concrete’s tolerance of irradiation. The research described herein was focused on providing insights on the role of the mineralogical composition and the rocks’ nature regarding the loss of elastic properties in relation to irradiation-induced expansion. The proposed modeling approach relies on the homogenization theory of random crystalline mediums.

2 Neutron-irradiated rocks data

2.1 Nature and chemical composition

The experimental data used in this analysis are provided by the Russian literature collected by Denisov et al. [22]. 27 magmatic rocks and 8 silicate- or carbonate-bearing sedimentary rocks were irradiated in different Russian test reactors—identified as AM, BR-5, BR-10, and BOR-60—at varied fluence levels and irradiation temperatures. All fluence data were normalized by Denisov et al. to a threshold of 10 keV according to the different reactors’ neutron spectra. The compositions of the magmatic (or igneous) rocks (# 1–27) are provided in Table 4. Felsic igneous rock (with high contents of quartz and feldspars) compositions are plotted within the quartz, alkali feldspar, plagioclase, feldspathoid (QAPF) double-ternary diagram [24] presented in Fig. 1, including granites and granodiorites (# 1–7), quartzitic andesite (# 9), diorites (# 10–12), urtite (# 13), gabbros, diabases, and basalts (# 14–20). For the sake of a convenient representation, the two silicate-bearing sedimentary aggregates, laminated aleurolite (# 28) and sandstone (# 29), are of mineral composition comparable to irradiated magmatic rocks and were also incorporated in this figure. Mafic igneous rock compositions are represented in Fig. 2, including pyroxenite (# 22), dunites (# 23–24), and hornblendite (#27). The remaining rock samples (# 30–35) are classified as carbonates, including two high-calcite limestones (# 30–31) and a dolimitic limestone (# 32: 20% dolomite). The other three irradiated sedimentary carbonates correspond to magnesite (# 33), 10%-quartz siderite (# 34), and dolomite (# 35).
2.2 Radiation-induced volumetric expansion

Denisov et al. gathered RIVE data for 132 aggregates provided in the form of RIVE-fluence plots with indications of the average irradiation temperatures. All plots have been digitized, and the extracted data were recorded in the irradiated minerals, aggregate and concrete (IMAC) database. The RIVE data are distributed as follows (numbers in parenthesis indicate the number of available RIVE data): granites (21), basalt (4), pyroxenites (3), sandstones (4) [25–32], granodiorites (5), liparite (3), quartzitic andesite (2), albatite (3), labradorite (10), urtite (3), diabases (13), peridotite (4), dunites (12), hornblendite (7) [28, 30–32], diorites (4), gabbros (10) [25, 27–32], magnesite (4), siderite (4) [30], and dolomite (2) [30, 33, 34]. The data cover a wide range of neutron fluences (<7 $n_{\text{E}}^{\text{e}} >^{10\text{keV}} \text{pm}^{-2}$) and irradiation temperatures (<350°C)—Fig. 3.

2.3 Elastic modulus

The dynamic elastic modulus of pristine and irradiated rocks were measured by ultrasonic pulse velocity and the data from a table extracted from Denisov’s work [22, Tab. 3.6.], which provides only a range of loss of mechanical properties for a given range of irradiation temperature and fluence for each rock. The hypothesis
in this work is that the loss of modulus is governed by
the rock-forming RIVE and the resulting mismatch
strain between mineral grains of varied orientations
and compositions. Hence, because of thermal anneal-
ing \([12, 35, 36]\) in neutron-irradiated crystallin min-
erals, it was assumed that the maximum loss of elastic
properties of irradiated rocks corresponds to the
highest irradiation fluence at the lowest temperature
and highest fluence, whereas the minimum loss occurs
at the highest temperature and lowest fluence. There-
fore, each given range of fluence and irradiation
temperature provides two data points (numbers in
parentheses indicate the number of available RIVE
data): (i) Igneous rocks: granite (12), graniodorite (4),
liparite (2), obsidian (2), diorite (4), quartzitic andesite
(4), trachesite andesite (4), albitite (2), labradorite (4),
urtite (2), gabbro (2), diabase (6), basalt (8),
pyroxenite (8), peridotite (2) hornblende (2), olivi-
nite (2) dunite (8), serpentinized dunite (4); (ii) Sedimentary rocks: aleurolite (6), sandstone (2),
quartzitic sandstone (4), calcium-bearing limestone
(6), other limestones (4) dolomite (4), magnesite (4),
siderite (4); (iii) Metamorphic rocks: hornstone (2),
serpentinite (6). Ores are not considered in this study.
While the RIVE data distinguish between different
rock compositions, the elastic modulus data do not.
The loss of mechanical properties data is assumed to
be relevant for all rocks belonging to the same class.
The irradiation conditions corresponding to the irra-
diated aggregates’ Young’s modulus data are presented in
Fig. 4. The corresponding range of fluences and
irradiation temperatures are comparable to the RIVE
data.

Fig. 2 Classification of mafic irradiated rocks based on the Px–
Ol–Hbl (left) and Cpx–Ol–Opx (right) diagrams of the IUGS
with mafic minerals \( \geq 90\% \). a Px–Ol–Hbl aggregate classification
diagram. b Cpx–Ol–Opx aggregate classification diagram.

Fig. 3 a Irradiation exposures (fluence and temperature) corresponding
to the 132 RIVE data available for this study \([22]\). Vertical bars indicate the
irradiation temperature ranges. b The colors (red, blue, and green) are directly
derived from SiO\(_2\) and –
CO\(_3\) and the “other oxides” ternary diagram of the 35
tested aggregates. (Color figure online)
3 Methodology

In this work, the interpretation of the RIVE and loss of elastic properties in irradiated rocks are derived using an upscaling approach. Only limited information about the rocks’ mineral compositions (volume fractions with an uncertainties estimated around \( \pm 5\% \)) and the average grain size are provided by Denisov et al. Hence, the proposed upscaling strategy is also limited to the homogenization theory of random polycrystalline mediums. Neutron-irradiation of rock-forming minerals causes the amorphization or metamictization of their pristine crystalline structures [12], which generally results in (1) a change of density [12, 22, 37], (2) the isotropization of its elastic tensor [18, 38], a change of apparent elastic modulus [18, 20, 38, 39], and (3) a change of chemical durability [15–17].

3.1 Minerals’ RIVE

The minerals’ tolerance against irradiation [21] and RIVE [22, 23] varies considerably with the chemical composition and the crystalline structures of the minerals. Details can be found in an article by Le Pape et al. [23]. In summary, at complete amorphization, carbonated minerals exhibit less RIVE (< \( \sim 1\% \)) than metal oxides (< \( \sim 5\% \)) and silicate-bearing minerals (< 18%). Important variations of RIVE are observed with silicated minerals: higher RIVEs are observed in highly percolated silicate structures (e.g., framework/tectosilicates such as quartz and feldspars) with higher silica content and Si–O bonds, whereas lower RIVEs occur when isolated SiO₄ is present (e.g., island/orthosilicates), thus increasing the number of ionic bonds. The absence of highly covalent bonds in carbonated minerals is also the main reason for their low RIVEs [15]. Not only the final volumetric expansion varies with the mineralogy, but the expansion rate also varies and is a function of the cumulated fluence level and the irradiation temperature governing the annealing effects [36, 37]. In a previous work, Le Pape et al. [23] have established empirical RIVE models for different mineral groups, mathematically described in the form of \( \varepsilon^* = \mathcal{F}(\Phi, T) \), where \( \varepsilon^* \) is the volumetric expansion, \( \Phi \) the cumulated fluence, and \( T \) is the average irradiation temperature. \( \mathcal{F} \) is a monotonic function of fluence, often sigmoidal, which expansion rate decreases with higher irradiation temperature. The details of the varied forms of \( \mathcal{F} \) can be found in section 2.1. of reference [23]. For each mineral group, the parameters governing \( \mathcal{F} \) were best-fitted on a set of nearly 400 data points collected originally by Denisov [22]. The possibility of nonuniform amorphization within a specific rock-forming mineral grain is not considered here. Mineral RIVE is assumed to produce isotropic dimensional change.

3.2 Elastic properties of minerals

The elastic properties of most common pristine rock-forming minerals are abundantly available in the public literature. The elastic constants are usually determined using acoustic wave propagation-based techniques such as the resonance frequency method. The number of independent elastic constants varies between 2 for an isotropic structure such as vitreous silica and 21 for a triclinic crystal such as albite. The corresponding elastic tensors for the minerals present in the aggregates reported in the Denisov study are reported in “Appendix 2”. The elastic properties of irradiated rock-forming minerals are insufficiently reported in the literature to develop a satisfactory model. Only the evolutions of the quartz elastic constants with fast neutron fluence have been comprehensively reported by Mayer and Lecomte [18], and partially by Zubov and Ivanov [38]. More recently, the apparent elastic properties of a chosen set of irradiated minerals were studied using molecular
dynamics (MD) simulations [20]. The neutron irradiation primary knock-out mechanism was modeled by ejecting constitutive minerals’ atoms at high kinetic energy until full amorphization was obtained. The Young’s modulus of the isotropic disordered mineral was compared to the apparent modulus of the equivalent random-oriented polycrystalline mineral. The Krishnan et al.’s study found the following variations of Young modulus: albite (framework silicate, feldspar group, NaAlSi3O8), −18%, almandine (nesosilicate, garnet group, Fe3Al2Si3O12), −42%, anorthite (framework silicate, feldspar group, CaAl2Si2O8), −5%, diopside (single-chain inosilicates, pyroxene group, MgCaSi2O6), −46%, enstatite (single-chain inosilicates, pyroxene group, MgSiO3), −26%, jadeite (single-chain inosilicates, pyroxene group, NaAlSi2O6), −57%, nepheline (framework silicate, feldspathoid group, NaAlSiO4 + 12%, and quartz (framework silicate, SiO2), +22%. An important change in stiffness between the pristine state and the fully disordered state occurs, including hardening in monocrystalline structures. However, in this work, the elastic constants of irradiated minerals are assumed constant and equal to those of the pristine materials due to the lack of data to support a validated model accounting for the evolution of the elastic constants of the irradiated minerals of interest. This limitation is addressed in the discussion.

3.3 Aggregate’s microstructures

Due to a lack of petrographic data, morphological information is limited to the volume fraction of the constitutive minerals. It is assumed that all rocks can be modeled by an assemblage of mineral polycrystals randomly oriented and defects such as cracks or pores modeled as oblate shapes with an aspect ratio varying between 0 (no-volume penny-shaped crack) and 1 (spherical pore). Those defects are introduced in the model to account for (1) the creation of volume during irradiation that is not accounted for by the cumulated volume change of the constitutive minerals and (2) for the loss of mechanical properties reported after irradiation. The mechanisms that initiate and cause development of voids and/or cracking during irradiation remain to be characterized. In this study, it is hypothesized that cracking occurs at the minerals’ grain boundaries because of the mismatch strains [40] caused by the differential radiation-induced expansion (Fig. 5). Mismatch strains can result from a difference in crystal orientation or a difference in mineral composition and structure. The “nano-voids” caused by the irradiation-induced amorphization are included in the model by the change of density of the irradiated minerals: that is, by the RIVE, which is assumed to occur uniformly for any given mineral grain.

3.4 Micromechanical model

3.4.1 Irradiated aggregate morphological and volume fractions model

An aggregate is modeled as a polycrystalline assemblage of minerals. Each cell of the polycrystal is homogeneously constituted from a single mineral and can randomly differ from other cells by its crystal orientation or by its constitutive mineral. In the case of porous aggregates, for the sake of simplicity, porosity is simply considered as an additional phase without stiffness. During irradiation, minerals are subject to expansion (RIVE). Due to the heterogeneities of both local stiffness and local expansion, so-called defects (cracks, additional porosity) are created. In this work, intergranular defects are considered to be forming at the interfaces between the polycrystal’s adjacent cells. A generic microstructure before and after irradiation is illustrated in Fig. 5.

Modeling the full extent of microstructural changes during irradiation—including local incompatible expansions, cracking, and defect growth—would be a tedious challenge requiring sophisticated nonlinear numerical models. Such approaches are being developed [41] in the context of energetic materials [42] which share some similarities with aggregates. Microstructure-wise, these energetic materials are polycrystals made up of only one grain type, with a few percent of binder phase. When exposed to temperature elevation, the heterogeneity of the thermal expansion tensor causes cracking due to crystallographic orientation mismatches. The local strains at stake are much smaller than in the irradiated aggregates case, but a first model has been proposed [41] to show crack development in a 2D polycrystal subjected to temperature elevation.

Alternatively, the simplified approach proposed herein only considers the initial pristine and final post-irradiation states. Furthermore, the final microstructure is considered sufficiently damaged so that
constitutive crystals can be considered free of any residual stresses which may have arisen as the result of incompatibilities of local expansions. The final microstructure can thus be described from volume balances, without any mechanical computation.

Each aggregate comprises \( N \) different types of minerals (each mineral occupies several cells of varied orientations) as denoted by the subscript \( i = 1, \ldots, N \). Subscripts \( a \) and \( d \) respectively denote the aggregate as a whole, as well as irradiation-induced defects. Volumes and volume fractions with respect to the aggregate are denoted as \( V \) and \( f \). The superscript 0 represents the initial pristine state, whereas the absence of a superscript denotes the final state. The RIVE of each mineral (estimated from model described in Sect. 3.1) and of the aggregate (experimental measurement) are denoted as \( e_i \) and \( e^*/C_3 \):

\[
\tilde{e}_i = \frac{V_i - V_i^0}{V_i^0}, \quad \text{and} \quad \tilde{e}^* = \frac{V_a - V_a^0}{V_a^0}.
\tag{1}
\]

The final volume of the constitutive minerals is as follows:

\[
\sum_{i=1}^{N} V_i = \sum_{i=1}^{N} V_i^0 (1 + \tilde{e}_i) = V_a^0 + V_a^0 \sum_{i=1}^{N} f_i^0 e_i = V_a^0 (1 + \tilde{e}^*), \tag{2}
\]

denoting \( \tilde{e}^* \) as the weighted (by initial volume fractions \( f_i^0 \)) average of mineral RIVE \( e_i \). The volume difference between the expanded aggregates and the expanded minerals is considered to be the irradiation-induced defects:

\[
V_a = V_a - \sum_{i=1}^{N} V_i = V_a^0 (\tilde{e}^* - \tilde{e}^*) = V_a^0 \Delta \phi, \tag{3}
\]

denoting \( \Delta \phi = \tilde{e}^* - \tilde{e}^* \) as the difference between the measured aggregate RIVE and the cumulated RIVE of minerals. The volume fraction of defects, \( f_d \), in the final post-irradiation state is then obtained by dividing by the final aggregate volume:

\[
f_d = \frac{V_d}{V_a} = \frac{\Delta \phi}{1 + \tilde{e}^* + \Delta \phi}. \tag{4}
\]

The final volume fraction of each mineral is straightforwardly obtained from Eq. (1):

\[
f_i = \frac{V_i}{V_a} = f_i^0 \frac{1 + \tilde{e}_i}{1 + \tilde{e}^* + \Delta \phi}. \tag{5}
\]

Volume fractions of minerals and defects in the irradiated aggregate can thus be estimated using these two equations, along with the volume fractions in the pristine aggregate and RIVE of minerals and \( \Delta \phi \). The latter can be deduced from the aggregate RIVE when it is known, or, following a more predictive approach, it can be estimated using the strategy described in Sect. 4.1.

The approach described above to estimate the amount of defects does not take into account the initial microstructure of aggregates, and does not model microstructural changes during irradiation. It is thus a simplified approach, which only yields an estimate of the volume fraction of defects. Modeling cracks and voids’ gradual development within the aggregates’ microstructure as irradiation proceeds would be a tedious challenge. However, the authors recognize

Fig. 5 Schematic representation of aggregate microstructure before and after irradiation exposure for \( N = 4 \) mineral phases (2D representation of 3D models)
that it would provide both refined estimates of the amount of irradiation-induced defects and valuable insights on their location.

### 3.4.2 Irradiated aggregate homogenization scheme

Estimating the effective post-irradiation stiffness of aggregates requires a so-called homogenization scheme. Among the available schemes, the self-consistent scheme [43–45] is the most suited to represent a polycrystalline assemblage. As only intergranular defects are considered, they are modeled at the same scale as the mineral cells, as an additional \((N+1)\)th phase. The self-consistent scheme is thus implemented following these assumptions: (1) each mineral cell is represented by a sphere, (2) each defect is represented by an oblate spheroid with a unique aspect ratio for all defects, (3) for each mineral phase, the distribution of the crystals’ orientations is assumed isotropic, (i.e., randomly distributed), and (4) the orientation of defects is also isotropically distributed. Thus, the effective stiffness of any aggregate is also isotropic. In summary, the effective elastic moduli of irradiated aggregates are derived by the self-consistent scheme as functions of the minerals’ stiffness tensors and the volume fractions of minerals and defects at the final state. “Appendix 1” provides the mathematical details of the micromechanical model. In particular, Eq. (19) presents the estimate of the elastic tensor of the irradiated aggregates in a compact form. To estimate the relative (irradiated with respect to pristine state) Young’s modulus, the initial Young’s modulus is computed by resorting to the same self-consistent scheme with the initial volume fractions of minerals and no defects (corresponding to the microstructure shown on the left in Fig. 5).

As the self-consistent scheme represents microstructure in an "implicit" way, it is important to validate its estimates with respect to numerical computations on explicit microstructures. In the context of energetic materials, Gasnier et al. [46] recently developed a similar self-consistent scheme using penny-shaped cracks instead of oblate defects. The estimated effective stiffness has been compared [46, 47] to numerical computations on microstructures reconstructed from several morphological assumptions regarding cracks and grains. The self-consistent scheme is found to accurately estimate effective moduli in the cases of cracked materials with (1) isotropic grains [47] or (2) moderately anisotropic grains when cracks are either transgranular [46] or superimposed to the polycrystalline tessellation [47]. When cracks are intergranular (separating two grains), the self-consistent scheme is found to over-estimate the effective moduli computed numerically in the cases investigated by Gasnier et al. [46]. These comparisons support the concept that mean field techniques have difficulties imposing the specific locations of inhomogeneities, cracks between two grains, for example. Sevostianov and Kachanov [48] propose to modify the differential scheme in this respect, but their approach is limited to isotropic grains.

Nevertheless, the self-consistent scheme is used here in the context of irradiated aggregates for the sake of simplicity. Approximations introduced by this scheme must be considered with the approximations on input data and without knowledge of the precise microstructures of irradiated aggregates.

### 4 Results

#### 4.1 Radiation-induced volumetric expansion of aggregates

The theoretical expansion of irradiated aggregates, \(\hat{\varepsilon}^r\), is first calculated accounting only for the cumulated contribution of the constitutive minerals’ RIVEs. The calculated expansions are then compared with the post-irradiation examination data, \(\dot{e}^r\), provided by Denisov et al. [22] as presented in Fig. 6. Each mark corresponds to a specific irradiation experiment. The colors of the marks are based on the mineral composition using the ternary silica-carbonate-other oxide diagram: red, blue and green indicate high-silica, high carbonate, and high metallic oxide contents, respectively. The size of each mark indicates its average grain size. The number associated with a mark corresponds to the aggregate’s label in Table 5. The theoretical RIVEs range between 0 and \(~ 9.5\%\), while the experimental RIVEs range between \(~ 5\%\) and \(< 25\%\). In general, the theoretical RIVEs tend to underestimate the experimental values, which supports the hypothesis of additional volume creation. For the sake of simplicity, the data can be subdivided into three groups: low-cracking (green shaded area), moderate cracking (yellow shaded area) high-cracking
It is remarkable that the data points corresponding to high-cracking have a high content of silica, which confirms recent results obtained by Maruyama et al. [49]. It can be observed that the RIVEs of rich metal oxide-bearing aggregates do not exceed 10%, which is in agreement with the lower RIVEs of such minerals. The RIVEs of rocks with high content carbonate contents remains low, with the exception of aggregate #34, which contains nearly 10% quartz.

The additional void creation \( \Delta \phi = \varepsilon^* - \varepsilon^c \) is calculated for each irradiation experiment’s data. Based on the first interpretation of Fig. 6, the data set was subdivided into three different groups according to their respective silica contents: a high silica content of > 65%, an intermediate silica content between 20% and 65% (relatively rich in metal oxides), and a low silica content of < 20%, which corresponds to carbonated aggregates. Figures 7a, 8a and 9a show the additional void creation against the experimental RIVE for the three groups. It can be seen that \( \Delta \phi \) and \( \varepsilon^c \) are linearly correlated. The corresponding equations are provided in the figures referenced above. The creation of defects (voids or cracks) occurs concurrently with the expansion of the aggregate-forming minerals. From a modeling perspective, the description of this process would need to be performed in the framework of nonlinear mechanics. In this work, the objective is focused on developing empirical models describing the final state following the irradiation experiment. Hence, alternatively, the void creation is estimated on an upper bound basis: \( \text{sup}(\Delta \phi) \), derived directly from the theoretical expansion \( \varepsilon^c \) of the uncracked aggregates. The analysis of the porosity increase against the theoretical expansion of the uncracked aggregates leads to postulation of the following linear relation: \( \text{sup}(\Delta \phi) \sim \eta \varepsilon^c \). The values of \( \eta \) for each aggregate group are 1.86 (Fig. 7b) for the high silica content group, 3.00, (Fig. 8b) for the intermediate silica content group, and 9.00 (Fig. 9b) for the low silica content group. The decrease of \( \eta \) with the increase of silica content may seem counterintuitive since higher RIVE is observed in minerals rich in silica, such as quartz. However, it can be hypothesized that the creation of voids results from the difference of RIVEs between the constitutive minerals causing

![Fig. 6 Comparison of experimental RIVE and cumulated expansion of rock-forming minerals](image-url)
crack formation. This crack formation is induced by mismatch strain occurring between minerals with different natures and crystal orientations [40]. This effect is illustrated by the aggregate #34 containing 10% of highly expansive (18% at complete amorphization) quartz within a siderite matrix (Fe$_{2}$CO$_{3}$) with a very low expansion potential 0.55%–0.7% [23].

4.2 Young’s modulus of irradiated aggregates

The void creation causes degradation of the mechanical properties of the irradiated aggregates. However, the loss of elastic properties depends not only on the volume fraction of voids, but also on the morphology of these voids, which are described by the oblate-shaped cracks governed by a unique aspect ratio.

The effective stiffness of exposed aggregate depends on the aspect ratio adopted to model the defects. To illustrate this dependence, 3 aggregates and exposure conditions are selected. The volume fraction of defects is evaluated according to (4) and is reported in Table 1. The influence of the defects’ aspect ratio on Young’s modulus reduction is plotted in Fig. 10. The residual Young’s modulus is smaller for flatter defects. As expected, the residual Young’s modulus
modulus is also smaller for higher volume fractions of defects.

For each aggregate group, an independent aspect ratio of defects is identified to reproduce the relation between the loss of modulus and the aggregate RIVE as closely as possible. Experimental data presented in Sect. 2.3 are used as reference. As these data are rather scattered, a straightforward decreasing exponential evolution is introduced:

$$\frac{E^*}{E_0} = e^{-\eta \frac{e}{C^0}}$$

where $\eta_{\text{ref}}$ is a “reference” characteristic aggregate RIVE.

For each aggregate group, the aspect ratio of defects is fit following this procedure:

- A characteristic RIVE $e_{\text{ref}}^{\exp}$ is identified based on reference experimental data (RIVE, relative Young’s modulus) as presented in Sect. 2.3.
- For irradiated aggregates collected as described in Sect. 2.2, the upper bound on additional voids $\Delta \phi = \eta \bar{\phi}$ (see Sect. 4.1) is taken as an estimate. Note that the measured aggregate RIVE is not used here. Volume fractions of minerals and defects in the irradiated configuration are calculated according to Eqs. (5) and (4). The homogenization procedure described in Sect. 3.4.2 is then used to estimate the loss of Young’s modulus, depending on the defect’s aspect ratio. The aspect ratio is

![Fig. 9](image1)

**Fig. 9** Theoretical porosity increase compared to the experiment RIVE (a) and the cumulated expansion of rock-forming minerals (b) for aggregates of silica content < 20% (c)

![Fig. 10](image2)

**Fig. 10** Influence of defects’ aspect ratio on estimated Young’s modulus reduction ($E_0$ denoting the Young’s modulus estimated before exposure, without defects)

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**Table 1** Details on selected aggregates and conditions

| Id   | Name                              | $T$ (°C) | Fluence (n/pm²) | $f_d$       |
|------|-----------------------------------|----------|-----------------|-------------|
| #6   | Medium-grain granodiorite         | 145      | 5.96            | $1.1 \times 10^{-1}$ |
| #13  | Large-grain urtite (nephelinic syenite) | 95       | 1.59            | $5.8 \times 10^{-3}$ |
| #35  | Medium-grain dolomite             | 145      | 5.98            | $2.1 \times 10^{-2}$ |
identified by minimizing the distance with respect to experimental data represented by Eq. \((6)\), with \(e_{\text{ref}} = e_{\text{exp}}\).

For reference purposes, another characteristic RIVE \(e_{\text{mod}}^{\text{ref}}\) is identified based on modeled data (RIVE, relative Young’s modulus).

Results are provided in Table 2. The identified aspect ratios are of the same order of magnitude and correspond to flat, crack-like defects. Finding the same order of magnitude for each aggregate group supports the fact that the main features of the irradiated morphology are similar. Differences lie in the volume fractions of defects, which depend on the specific constitutive minerals and the exposure conditions.

The loss of mechanical properties of irradiated aggregates is illustrated by the evolution of the relative Young’s modulus with the RIVE shown in Figs. 11, 12, and 13 for the three groups of rocks. The relative Young’s modulus exhibits an exponential-like decrease with the RIVE. Such behavior is qualitatively comparable to the loss of elastic properties caused by alkali-silica reaction-induced swelling \([50]\).
Fig. 14 Loss of elastic modulus of aggregates with the amorphization index. The red, green, and blue solid lines correspond to the fitting curves using the expression $E^*/E_0 = \exp(-\alpha \epsilon^*/\epsilon^*_{\text{max}})$, respectively for $[\text{SiO}_2] \geq 65\%$, $20\% \leq [\text{SiO}_2] \leq 65\%$, and $[\text{SiO}_2] \leq 20\%$. (Color figure online)

decreasing trend is fitted using the following mathematical expression: $E^*/E_0 \approx \exp[-\beta(\epsilon^* + \sup \Delta \phi)]$, where $E^*$ is the Young’s modulus of the irradiated material, and $E_0$ is its pristine value. The values of $\beta$ increase when the silica-content decreases, indicating that for an equivalent expansion level, the extent of damage substantially increases for lower content silicate-bearing aggregates: $\beta = 47.1$ for $[\text{SiO}_2] > 65\%$, $\beta = 53.1$ for $25\% < [\text{SiO}_2] < 65\%$, and $\beta = 79.3$ for $[\text{SiO}_2] < 20\%$. This trend can be put in perspective, with the evolution of $\eta$ supporting the hypothesis of higher damage development in aggregates formed with different minerals subjected to contrasted RIVEs.

5 Discussion

5.1 Contribution of the elastic tensors in irradiated minerals

Due to the lack of data, the assumption made in this study is that the elastic tensors of the irradiated minerals do not change with gradual amorphization. Based on the results, which were mainly obtained using first principle–based simulation on a limited set of silicates, the stiffness of the irradiated silicates at full amorphization appears to decrease in a range of $-5\%$ to nearly $-50\%$ except in two framework silicates, quartz and nepheline, in which stiffness increases by $+20\%$ and $+10\%$, respectively. It should be emphasized that these values are relevant for the final stage of the amorphization process, which corresponds to high RIVEs occurring at high levels of fluence. Tentatively, the amorphization index ($\in [0;1]$) is approached with the relative expansion to the maximum RIVE, $\hat{\epsilon}^* / \hat{\epsilon}^*_{\text{max}}$, as derived from the mineral contents of the aggregates. Figure 14 presents the evolution of the loss of Young’s modulus with the amorphization index. It can be observed that the calculated loss of Young’s modulus evolves differently with the aggregates’ silica content. The effective modulus of the poly-crystalline assemblage of minerals results from the contribution of (1) The evolution of the stiffness tensors of its constitutive minerals caused by irradiation-induced defects at the atomistic scale, and (2) The formation of defects at the mesoscale (e.g., at the grain boundary) caused by mismatch expansions between different minerals as proposed in our model. For high content of silica ($[\text{SiO}_2] \geq 65\%$), it reaches its maximum value for relative expansion between about 20 and 40%. In that case, it can be hypothesized that early-stage mismatch expansions of the constitutive minerals cause substantial internal mechanical damage. The contribution of the irradiation-induced change of the minerals’ elastic constants to the Young’s modulus of aggregates with $[\text{SiO}_2] \geq 65\%$ is of lesser importance. As the silica content decreases, the rate of Young’s modulus loss with the amorphization index is not as sharp. For that type of aggregate ($20\% \leq [\text{SiO}_2] \leq 65\%$), it is possible that the changing irradiated minerals’ elastic properties interact with the RIVE-induced mismatch strains, causing damage, and contributing to the effective loss of stiffness in the aggregates. For carbonated aggregates, most data correspond to a state of complete amorphization, making it difficult to draw conclusions. Detailed examination and damage characterization of irradiated rocks are needed in the future to study this question further.

5.2 Role of the average grain size

While detailed information about the microstructures of the tested rocks is not available, the average grain size of each rock is provided by Denisov et al. Theoretically, the formation of misfit strain ($\Delta e$)-
induced cracking onset at the grain boundary depends on the grain size \( l \) [40, 51]: \( \Delta \varepsilon \propto l^{-1/2} \). Figure 15 presents the estimated contribution of irradiation-induced void creation to the experimental RIVE, \( \Delta \Phi / \varepsilon' \), plotted as a function of the aggregates’ silica content [SiO₂] and the aggregates’ average grain size for all the RIVE data available in this study. For aggregates of similar silica content, no clear trend regarding the role of the average grain size on the irradiation-induced void formation can be drawn. Once more, only thorough characterization of the irradiation-induced damage in rocks will make it possible to clearly understand the nature, scale and development of defects and voids in rocks of varied natures.

5.3 Influence of the silica-content on irradiation-induced damage

The nature of irradiation-induced damage in concrete-forming aggregates varies with the observation scale.

At the atomistic scale, fast neutron-irradiation causes mainly ballistic effects in the form of cascading knock-on atoms. However, the impact of cumulated cascades on the effective physical and mechanical properties of irradiated aggregate-forming minerals vary with their crystalline structures. Covalent bonds are highly directional and rigid. Hence, the atoms surrounding knock-on position are subject to displacement caused by the crystals’ lattice deformation and broken bonds are unlikely to reform [10, 15]. Conversely, in the presence of less directional and rigid ionic bonds, knock-on atoms are displaced more independently of the surrounding crystal lattice and broken bonds are more likely to reform. In consequence, minerals RIVE increases with the number of covalent bonds and the silicates tetrahedrons structures. For example, this explains why quartz, a fully-covalent tecto-silicate exhibits a maximum RIVE one order of magnitude higher than olivine [22], a highly ionic ortho-silicate 25% of Si–O bonds [21]. Note that the silica content does not provide a good indication of the irradiation tolerance of silicates [21, 23].

At the meso-scale, aggregates can be described as a polycrystalline assemblage of varied minerals which exhibit varied RIVEs and mechanical properties. In this study, aggregates were classified by their oxides contents, and more specifically by their SiO₂ content.

(a) Complete data set. (b) Reduced data set around irradiation condition of \( \sim 1n^8 > 10^{4} \text{ pm}^{-2} \) and 100°C. The same color chart representing the aggregates’ mineral composition as for the other figures is used here. (Color figure online)
At this scale, the irradiation-induced defects hypothetically correspond to the formation of voids, cracks and grains boundary debonding caused by mismatch strains between adjacent irradiated minerals. The defects are characterized by the loss of the effective elastic modulus. In this study, it is found that the silica-content acts differently on RIVE and on residual mechanical properties. High silica-content aggregates tend to exhibits higher expansions mainly because of a higher content of quartz, confirming Maruyama et al.’s findings [49]. However, and almost counter-intuitively, the loss of elastic properties is sharper for lower silica-content aggregates than for higher silica-content aggregates at comparable RIVE. Without accessible data on post-irradiation examination of the aggregates, only hypothesis can be drawn. The authors’ assumption is that lower silica-content aggregates are subject to greater mismatch strain between the constitutive mineral phases as discussed in the previous section.

6 Conclusion

In this study, historical irradiation data of concrete-forming aggregates were revisited with the objective of analyzing the effects of neutron irradiation on their induced expansion and their loss of mechanical properties. The approach is derived from a polycrystalline micromechanical model (self-consistent scheme). To the authors’ knowledge, this is the first model ever developed for estimating the expansion and elastic properties of irradiated rocks based only on their mineral composition and their pristine Young’s moduli. From this analysis, it can be inferred that: (1) the post-irradiation expansion of aggregates is caused by the contribution of its rock-forming minerals and the formation of additional voids, the exact nature of which remains to be determined; (2) silicate-bearing aggregates are subjected to higher expansions than carbonate-bearing aggregates due to the higher inclination towards high RIVEs in tectosilicates such as quartz and feldspars; (3) however, it was found that, on average, the relative increase of defects was larger for aggregates of lower silica content at comparable theoretical expansions of the constitutive minerals; (4) the loss of Young’s modulus of irradiated aggregates is correlated to their RIVEs with a trend which can be represented by an exponential decrease; and (5) at comparable RIVEs, the loss of Young’s modulus is, on average, more important for aggregates with lower silica content. Hence, it is inferred that the irradiation-induced damage rate (void creation rate) is higher in aggregates with lower amounts of silica. It can be hypothesized that damage formation is driven by the strains’ mismatch between adjacent minerals. With that assumption, the highest damage rate would correspond to an aggregate containing quartz embedded in a carbonated mineral matrix. The practical implications of these findings are described here.

For operating light water reactors, the nature of the aggregates is critical regarding their tolerance against prolonged irradiation. In addition to the determination of the irradiation conditions (flux, fluence and temperature) using irradiation transport models, characterizing the mineralogy of the constitutive aggregates used for the construction of the biological shield is a necessary prerequisite to the sound assessment of the risk of degradation of the irradiated concrete shielding the reactor. For the construction of the biological shield of new reactors, it is recommended that carbonated rocks such as limestone or dolomite be used rather than igneous rocks such as granite, for example. However, even when using carbonated rocks, a careful characterization of the aggregates must be conducted to detect the presence of deleterious silicates such as quartz. The presence of more vitreous forms such as chert or flint is far less problematic because of their poorly crystallized structures causing less RIVE, if not moderate contractions.

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Compliance with ethical standards

Conflicts of interest The authors declare that they have no conflict of interest.

Appendix

Micromechanics equations

First, the general framework of homogenization of random media in linear elasticity is recalled. Then, the
self-consistent scheme used to estimate irradiated aggregates stiffness is briefly derived. For more
details, see Zaoui and Dormieux et al. [52, 53].

Introduction to homogenization of random media

A representative elementary volume (REV), occupying the domain \( \Omega \), of composite material is considered. Its
local behavior is linear elastic with a heterogeneous
stiffness tensor \( C(x) \):

\[
\sigma(x) = C(x) : \varepsilon(x)
\]

(7)

An average macroscopic strain \( E \) is imposed to this domain through kinematic uniform boundary conditions.
More precisely, the displacement field \( \xi(x) \) is prescribed on the boundary \( \partial \Omega \) of the REV, as:

\[
\xi(x) = E : x, \ x \in \partial \Omega
\]

(8)

These boundary conditions ensure that the average \( \langle \varepsilon(x) \rangle \) of the strain field arising in the REV is equal to \( E \). This strain field linearly depends on the macroscopic strain due to the linearity of the equations defining the elastic problem:

\[
\varepsilon(x) = \lambda_i(x) : E
\]

(9)

Introducing the so-called strain localization tensor \( \lambda_i(x) \), the macroscopic stress is then obtained by spatially averaging the microscopic stress:

\[
\Sigma = \langle \sigma(x) \rangle = \frac{1}{|\Omega|} \int_{\Omega} \sigma(x) \, d\Omega
\]

(10)

The effective stiffness is then defined as the tensor relating the macroscopic stress \( \Sigma \) to the macroscopic strain \( E \):

\[
C_{\text{eff}} = \langle C(x) : \lambda_i(x) \rangle
\]

(11)

When the composite material can be split into phases (domains in which the stiffness tensor is uniform),
then this expression becomes:

\[
C_{\text{eff}} = \sum_i f_i C_i : \langle \lambda_i(x) \rangle_i
\]

(12)

\( i \) iterating over phases. Thus, the complete determination of the strain localization tensor field is not
necessary: only averages over each phase are required.

Starting from a statistical description of the morphology, these averages can be estimated by taking
advantage of so-called homogenization schemes.

Derivation of the self-consistent scheme

The specific case of a polycrystalline material is now considered, with \( N + 1 \) phases. Each phase is charac-
terized by a crystal shape and an anisotropic stiffness
tensor. Each phase is present as many different
crystals, differing only by crystallographic orientation,
the orientation distribution being isotropic. The
effective stiffness is thus isotropic.

For a given crystal of phase \( i \) whose crystallographic orientation is denoted \( \theta \), the stiffness tensor is
denoted \( C_{i, \theta} \). The average strain over all crystals of
the same phase and having the same orientation in the
REV is classically estimated as the strain arising in a
single particle embedded into the sought effective
medium (stiffness \( C_{\text{SC}} \)), with kinematic uniform
boundary conditions \( \Sigma^0 \). This is the well-known
Eshelby inhomogeneity problem [54], for which the solution is:

\[
\langle \varepsilon \rangle_{i, \theta} = \left( \mathbb{I} + \mathbb{P}_{i, \theta}^{\text{SC}} : (C_{i, \theta} - C_{\text{SC}}) \right)^{-1} : E^0
\]

(13)

The Hill tensor \( \mathbb{P}_{i, \theta}^{\text{SC}} \) depends on the embedding
medium stiffness \( C_{\text{SC}} \) and on the shape of the particle
representing orientation \( \theta \) and phase \( i \). This shape is
spherical for minerals (\( i = 1..N \)) and oblate spheroidal
for defects (\( i = N + 1 \)). In both cases, and with an
isotropic stiffness \( C_{\text{SC}} \), the Hill tensor has an analytical
expression, which can be found for example in [53].
These expressions are recalled in Sect. 1, for completeness
purposes.

The average strain over all crystals of phase \( i \) is then
obtained by angular average, considering the isotropic
orientation distribution:

\[
\langle \varepsilon \rangle_i = \left\langle \mathbb{I} + \mathbb{P}^{\text{SC}}_{i, \theta} : (C_{i, \theta} - C_{\text{SC}}) \right\rangle_{\theta}^{-1} : E^0
\]

(14)

the averaging operator \( \langle \rangle_{\theta} \) being defined by:

\[
\langle \mathbb{T}_{\theta} \rangle_{\theta} = \int_0^\pi \int_0^{2\pi} \int_0^{2\pi} \mathbb{T}(\theta, \phi, \psi) \sin \theta \, d\psi \, d\phi \, d\theta
\]

(15)

with angles \( \theta, \phi, \) and \( \psi \) characterizing orientation
of the crystal frame with respect to the reference frame.
Then, Eq. (11) is used to derive the effective stiffness tensor:

\[ C^{SC} = \left( \sum_{i=1}^{N+1} f_i \left( 1 + \mathbb{P}_{i,or}^{SC} : (C_{i,or} - C^{SC}) \right)^{-1} \right)_{or} \]

(19)

This tensorial equation, projected over \( \mathbb{T} \) and \( \mathbb{K} \), yields two nonlinear equations, involving the effective bulk \( k^{SC} \) and shear \( \mu^{SC} \) moduli.

**Hill tensors expressions**

The Hill tensor for a sphere in an isotropic elastic medium (Young’s modulus \( E \) and Poisson’s ratio \( \nu \)) is itself isotropic:

\[ \mathbb{P}_{sph} = \frac{1 + \nu}{3E(1 - \nu)} \left( 1 - 2\nu \right) \mathbb{J} + \frac{2}{5} \left( 4 - 5\nu \right) \mathbb{K} \]

(20)

The Hill tensor for an oblate spheroid (aspect ratio \( \rho < 1 \)) in an isotropic elastic medium is transversely isotropic with major symmetry. In the frame associated to the spheroid axes (\( \mathbb{u}_3 \) being the axis of revolution), its components in Mandel-Voigt notation are:

\[
\begin{bmatrix}
P_{11} & P_{12} & P_{13} & 0 & 0 & 0 \\
0 & 0 & 0 & P_{22} & 0 & 0 \\
0 & 0 & 0 & 0 & P_{33} & 0 \\
\end{bmatrix}
\]

(21)

These 5 independent components are:

\[ P_{11}/P_0 = (4(4\nu - 1)\rho^2 + 13 - 16\nu)\alpha - 3\rho^2 \]

(22)

\[ P_{12}/P_0 = (4\rho^2 - 1)\alpha - \rho^2 \]

(23)

\[ P_{13}/P_0 = -4(2\rho^2 + 1)\alpha + 4\rho^2 \]

(24)

\[ P_{33}/P_0 = 8(1 - \nu)(4\nu - 1)\rho^2 + 4\nu - 1)\alpha + 8(2(\nu - 1)\rho^2 + 1 - 2\nu) \]

(25)
Table 3  Stiffness tensor of minerals in the IMAC database

| Phases          | Stiffness tensor mean$_{\text{mean}}^{\text{std}}$ | References |
|-----------------|--------------------------------------------------|------------|
| Albite (triclinic) | $\begin{bmatrix} 96.2^{(1)}_{\pm 0} & 46.1^{(1)}_{\pm 0} & 38.4^{(1)}_{\pm 0} & 5.9^{(1)}_{\pm 0} & 0.2^{(1)}_{\pm 0} & -0.2^{(1)}_{\pm 0} & -0.4^{(1)}_{\pm 0} \\ 112.5^{(1)}_{\pm 0} & 33.4^{(1)}_{\pm 0} & 33.4^{(1)}_{\pm 0} & 0.0 & 0.0 & 0.0 & 0.0 \\ 112.5^{(1)}_{\pm 0} & 33.4^{(1)}_{\pm 0} & 33.4^{(1)}_{\pm 0} & 0.0 & 0.0 & 0.0 & 0.0 \\ 29.9^{(1)}_{\pm 0} & 0.0 & 0.0 & 0.0 & 0.0 & 0.0 & 0.0 \\ 29.9^{(1)}_{\pm 0} & 0.0 & 0.0 & 0.0 & 0.0 & 0.0 & 0.0 \\
| Analcime (cubic) | $\begin{bmatrix} 71^{(9)}_{\pm 6.2} & 33.1^{(9)}_{\pm 5.4} & 32.6^{(9)}_{\pm 5.5} & 4.9^{(6)}_{\pm 1.2} & -2.3^{(9)}_{\pm 1.3} & 0.0 \\ 155.7^{(9)}_{\pm 20} & 17.8^{(9)}_{\pm 13} & -10.6^{(6)}_{\pm 3.3} & -9.4^{(9)}_{\pm 8.5} & -6.5^{(6)}_{\pm 1.6} & -6.5^{(6)}_{\pm 8.5} \\ 156^{(9)}_{\pm 21.3} & -1.3^{(6)}_{\pm 5.2} & 1.7^{(9)}_{\pm 12.2} & -6.5^{(6)}_{\pm 8.9} & -6.5^{(6)}_{\pm 8.9} \end{bmatrix}$ | [55–59] |
| Andesine (triclinic) | $\begin{bmatrix} 127^{(3)}_{\pm 4.6} & 62.8^{(3)}_{\pm 4.2} & 52.9^{(3)}_{\pm 2.4} & 9.4^{(2)}_{\pm 0.2} & -4.8^{(3)}_{\pm 12.5} & -9.6^{(2)}_{\pm 1.7} \\ 194.4^{(3)}_{\pm 14.2} & 35.5^{(3)}_{\pm 5.6} & 3.9^{(2)}_{\pm 5.1} & 1.3^{(3)}_{\pm 5.4} & -9.4^{(2)}_{\pm 3.1} & -9.4^{(2)}_{\pm 3.1} \\ 162^{(3)}_{\pm 5.8} & 10.2^{(2)}_{\pm 5.1} & -4.1^{(3)}_{\pm 12.5} & -3.9^{(2)}_{\pm 7.8} & -3.9^{(2)}_{\pm 7.8} \\ 23.9^{(3)}_{\pm 0.6} & 1.6^{(2)}_{\pm 2.1} & 1.3^{(3)}_{\pm 5.2} & 1.3^{(3)}_{\pm 5.2} & 1.3^{(3)}_{\pm 5.2} \\ 37.5^{(3)}_{\pm 2.5} & 2.7^{(2)}_{\pm 3.5} & 2.7^{(2)}_{\pm 3.5} & 2.7^{(2)}_{\pm 3.5} & 2.7^{(2)}_{\pm 3.5} \\ 39.6^{(3)}_{\pm 3.1} & 39.6^{(3)}_{\pm 3.1} & 39.6^{(3)}_{\pm 3.1} & 39.6^{(3)}_{\pm 3.1} & 39.6^{(3)}_{\pm 3.1} \end{bmatrix}$ | [55, 58, 59] |
| Phases                          | Stiffness tensor mean $\pm$ std | References |
|--------------------------------|---------------------------------|------------|
| Anorthoclase (triclinic)       |                                 | [59]       |
|                                | $\begin{bmatrix} 63^{(1)}_{\pm 0} & 38.4^{(1)}_{\pm 0} & 48.5^{(1)}_{\pm 0} & 0 & -12.5^{(1)}_{\pm 0} & 0 \\ 152.4^{(1)}_{\pm 0} & 35.7^{(1)}_{\pm 0} & 0 & -2.3^{(1)}_{\pm 0} & 0 \\ 117.6^{(1)}_{\pm 0} & 0 & -21.3^{(1)}_{\pm 0} & 0 \\ 9.9^{(1)}_{\pm 0} & 0 & -1.9^{(1)}_{\pm 0} & 0 \\ 26.9^{(1)}_{\pm 0} & 0 & & & \\ 35.4^{(1)}_{\pm 0} & & & & \end{bmatrix}$ |           |
| Augite (monoclinic)            |                                 | [62, 63]   |
|                                | $\begin{bmatrix} 180.8^{(2)}_{\pm 1.1} & 73.4^{(1)}_{\pm 0} & 72.4^{(1)}_{\pm 0} & 0 & 0 & 19.9^{(1)}_{\pm 0} \\ 150.4^{(2)}_{\pm 0.5} & 33.9^{(1)}_{\pm 0} & 0 & 0 & 16.6^{(1)}_{\pm 0} \\ 218.9^{(2)}_{\pm 1.6} & 0 & 0 & 24.5^{(1)}_{\pm 0} \\ 69.7^{(1)}_{\pm 0} & 4.3^{(1)}_{\pm 0} & 0 & 55.8^{(1)}_{\pm 0} \\ 51.1^{(1)}_{\pm 0} & & & & \end{bmatrix}$ |           |
| Biotite (hexagonal)            |                                 | [64]       |
|                                | $\begin{bmatrix} 186^{(1)}_{\pm 0} & 32.4^{(1)}_{\pm 0} & 11.6^{(1)}_{\pm 0} & 0 & 0 & 0 \\ 186^{(1)}_{\pm 0} & 11.6^{(1)}_{\pm 0} & 0 & 0 & 0 \\ 54^{(1)}_{\pm 0} & 0 & 0 & 0 \\ 5.8^{(1)}_{\pm 0} & 0 & 0 & 0 \\ 5.8^{(1)}_{\pm 0} & 0 & 0 & 0 \\ 76.8^{(0)}_{\pm 0} & & & & \end{bmatrix}$ |           |
| Bromellite (hexagonal)         |                                 | [65, 66]   |
|                                | $\begin{bmatrix} 465.3^{(2)}_{\pm 0.9} & 147.3^{(2)}_{\pm 0.3} & 103.8^{(2)}_{\pm 21.6} & 0 & 0 & 0 \\ 465.3^{(2)}_{\pm 0.6} & 103.8^{(2)}_{\pm 21.6} & 0 & 0 & 0 \\ 492.8^{(2)}_{\pm 1.7} & 0 & 0 & 0 \\ 153^{(1)}_{\pm 0} & 0 & 0 & 0 \\ 159^{(1)}_{\pm 0} & 0 & 0 & 0 \\ 159^{(0)}_{\pm 11.3} & & & & \end{bmatrix}$ |           |
| Bronzite (orthorhombic)        |                                 | [59, 67, 68]|
|                                | $\begin{bmatrix} 107.4^{(3)}_{\pm 3.5} & 69.4^{(2)}_{\pm 1.1} & 58.9^{(2)}_{\pm 2.3} & 0 & 0 & 0 \\ 161.9^{(3)}_{\pm 3.8} & 52.9^{(2)}_{\pm 4.6} & 0 & 0 & 0 \\ 195.1^{(3)}_{\pm 20.8} & 0 & 0 & 0 \\ 76.6^{(2)}_{\pm 9.3} & 0 & 0 & 0 \\ 67.8^{(2)}_{\pm 12.2} & 0 & & & \\ 66.5^{(2)}_{\pm 17.2} & & & & \end{bmatrix}$ |           |
| Phases               | Stiffness tensor mean$^{\text{min}}_{\pm \text{std}}$ | References |
|----------------------|-----------------------------------------------------|------------|
| Bytownite (triclinic) | $\begin{bmatrix} 120.4^{(1)}_{\pm 0} & 56.6^{(1)}_{\pm 0} & 49.9^{(1)}_{\pm 0} & 9^{(1)}_{\pm 0} & 3.2^{(1)}_{\pm 0} & -3^{(1)}_{\pm 0} \\ 191.6^{(1)}_{\pm 0} & 26.4^{(1)}_{\pm 0} & 2.1^{(1)}_{\pm 0} & 5.4^{(1)}_{\pm 0} & -9.5^{(1)}_{\pm 0} \\ 163.7^{(1)}_{\pm 0} & 1.7^{(1)}_{\pm 0} & 1.7^{(1)}_{\pm 0} & -8.1^{(1)}_{\pm 0} \\ 23.3^{(1)}_{\pm 0} & -0.8^{(1)}_{\pm 0} & 0.9^{(1)}_{\pm 0} \\ 32.8^{(1)}_{\pm 0} & 4.5^{(1)}_{\pm 0} \\ 35^{(1)}_{\pm 0} \end{bmatrix}$ | [58] |
| Calcite (hexagonal)  | $\begin{bmatrix} 146.1^{(7)}_{\pm 2} & 56^{(7)}_{\pm 1.5} & 52.5^{(7)}_{\pm 1.5} & 0 & 0 & 0 \\ 146.1^{(7)}_{\pm 2} & 52.5^{(7)}_{\pm 1.5} & 0 & 0 & 0 \\ 84.9^{(7)}_{\pm 0.7} & 0 & 0 & 0 \\ 33.5^{(7)}_{\pm 0.5} & 0 & 0 \\ 33.5^{(7)}_{\pm 0.5} & 0 \\ 45.1^{(0)}_{\pm 0} \end{bmatrix}$ | [61, 69–73] |
| Cassiterite (tetragonal) | $\begin{bmatrix} 261.7^{(1)}_{\pm 0} & 177.5^{(1)}_{\pm 0} & 155.5^{(1)}_{\pm 0} & 0 & 0 & 0 \\ 261.7^{(1)}_{\pm 0} & 155.5^{(1)}_{\pm 0} & 0 & 0 & 0 \\ 449.6^{(1)}_{\pm 0} & 0 & 0 & 0 \\ 103.1^{(1)}_{\pm 0} & 0 & 0 \\ 103.1^{(1)}_{\pm 0} & 0 \\ 207.4^{(1)}_{\pm 0} \end{bmatrix}$ | [74] |
| Clinohlore (monoclinic) | $\begin{bmatrix} 190.9^{(2)}_{\pm 10.2} & 63.1^{(2)}_{\pm 8.2} & 26.9^{(2)}_{\pm 18.2} & 0 & 0 & 0 \\ 197.7^{(1)}_{\pm 0} & 19.6^{(1)}_{\pm 0} & 0 & 0 & 0 \\ 117.5^{(2)}_{\pm 29.2} & 0 & 0 & 0 \\ 18.7^{(2)}_{\pm 10.2} & 0 & 0 \\ 24.6^{(1)}_{\pm 0} & 0 \\ 62.4^{(2)}_{\pm 12.2} \end{bmatrix}$ | [64, 75] |
| Cordierite (orthorhombic) | $\begin{bmatrix} 207.3^{(1)}_{\pm 0} & 93.7^{(1)}_{\pm 0} & 95.1^{(1)}_{\pm 0} & 0 & 0 & 0 \\ 213.6^{(1)}_{\pm 0} & 88.9^{(1)}_{\pm 0} & 0 & 0 & 0 \\ 186.1^{(1)}_{\pm 0} & 0 & 0 & 0 \\ 46.5^{(1)}_{\pm 0} & 0 & 0 \\ 51.6^{(1)}_{\pm 0} \\ 64^{(1)}_{\pm 0} \end{bmatrix}$ | [76] |
| Phases                  | Stiffness tensor mean$^{\text{min}}_{\text{std}}$ | References   |
|------------------------|---------------------------------------------|--------------|
| Corundum (trigonal)    | $\begin{bmatrix} 497.5_{\pm0.2} & 162.7_{\pm0.1} & 116.6_{\pm0.8} & -22.4_{\pm0.7} & 0 & 0 \\ 497.5_{\pm0.2} & 116.6_{\pm0.8} & 22.4_{\pm0.7} & 0 & 0 \\ 501.4_{\pm0.7} & 0 & 0 & 0 & 0 \\ 147_{\pm0.3} & 0 & 0 & 0 & -22.4_{\pm0.7} \\ 147_{\pm0.3} & 0 & 0 & 0 & 167.4_{\pm0.1} \end{bmatrix}$ | [77, 78] |
| Diopside (monoclinic)  | $\begin{bmatrix} 168.2_{\pm7.3} & 78.8_{\pm1.2} & 82.5_{\pm9.1} & 0 & 0 & -3.7_{\pm1.9} \\ 175.3_{\pm4.2} & 54.7_{\pm5.6} & 0 & 0 & -3.3_{\pm1.5} \\ 239.2_{\pm4.4} & 0 & 0 & 3.6_{\pm4.6} \\ 73.5_{\pm3.7} & -2.7_{\pm1.1} & 0 \\ 71.3_{\pm4.5} & 0 & 63.1_{\pm5.3} \end{bmatrix}$ | [59, 62, 79, 80] |
| Dolomite (trigonal)    | $\begin{bmatrix} 205.9_{\pm1.0} & 71_{\pm1.0} & 57.4_{\pm1.0} & -19.5_{\pm1.0} & 0 & 0 \\ 205.9_{\pm1.0} & 57.4_{\pm1.0} & 19.5_{\pm1.0} & 0 & 0 \\ 112.8_{\pm1.0} & 0 & 0 & 0 \\ 39.8_{\pm1.0} & 0 & 0 & 0 \\ 39.8_{\pm1.0} & -19.5_{\pm1.0} \\ 67.5_{\pm1.0} \end{bmatrix}$ | [81] |
| Enstatite (tetragonal) | $\begin{bmatrix} 286.4_{\pm1.0} & 83_{\pm1.0} & 104.9_{\pm1.0} & 0 & 0 & 1.4_{\pm1.0} \\ 286.4_{\pm1.0} & 104.9_{\pm1.0} & 0 & 0 & 0 & -1.4_{\pm1.0} \\ 280.1_{\pm1.0} & 0 & 0 & 0 \\ 85_{\pm1.0} & 0 & 0 \\ 85_{\pm1.0} & 0 & 101.7_{\pm1.0} \end{bmatrix}$ | [82] |
| Fluorapatite (hexagonal)| $\begin{bmatrix} 146.5_{\pm7.8} & 48_{\pm2.8} & 59.6_{\pm5.9} & 0 & 0 & 0 \\ 146.5_{\pm7.8} & 59.6_{\pm5.9} & 0 & 0 & 0 \\ 181.4_{\pm6.2} & 0 & 0 & 0 \\ 43.5_{\pm1.1} & 0 & 0 \\ 43.5_{\pm1.1} & 0 & 49.3_{\pm2.5} \end{bmatrix}$ | [83, 84] |
| Phases                     | Stiffness tensor mean \( \mu \) ± std. | References |
|---------------------------|----------------------------------------|------------|
| Forsterite (orthorhombic) | \[
\begin{bmatrix}
327.6 \pm 2.3 & 66 \pm 1 & 68.8 \pm 1.4 & 0 & 0 & 0 \\
198 \pm 4.7 & 73.1 \pm 1.3 & 0 & 0 & 0 \\
236.6 \pm 2.1 & 66.3 \pm 1.1 & 0 & 0 & 0 \\
80.8 \pm 1.3 & & & & & 80.5 \pm 0.9
\end{bmatrix}
\] | [85–90] |
| Hematite (hexagonal)      | \[
\begin{bmatrix}
355.9 \pm 0.1 & 185 \pm 0 & 209.4 \pm 0.1 & 0 & 0 & 0 \\
355.9 \pm 0.1 & 209.4 \pm 0.1 & 0 & 0 & 0 \\
299.2 \pm 0.1 & 58 \pm 0 & 0 & 0 & 0 \\
58 \pm 0 & & & & & 85.4 \pm 0
\end{bmatrix}
\] | [91] |
| Hornblende (monoclinic)   | \[
\begin{bmatrix}
115.9 \pm 0.1 & 47.1 \pm 2.1 & 62 \pm 2.1 & 0 & 0 & -0.6 \pm 0.9 \\
158.9 \pm 0.2 & 65.4 \pm 2.1 & 0 & 0 & -10.6 \pm 1.5 \\
191.5 \pm 0.2 & 0 & 0 & 0.7 \pm 1.3 \\
58.1 \pm 0 & -6.4 \pm 0.3 & 0 & 37.7 \pm 1.2 & 31.8 \pm 0.1
\end{bmatrix}
\] | [59, 70] |
| Hydroxylapatite (hexagonal) | \[
\begin{bmatrix}
140 \pm 1 & 13 \pm 0 & 69 \pm 1 & 0 & 0 & 0 \\
140 \pm 1 & 69 \pm 1 & 0 & 0 & 0 \\
180 \pm 1 & 0 & 0 & 0 & 0 \\
36.2 \pm 1 & 0 & 0 & 0 & 36.2 \pm 1 \\
& & & & & 63.5 \pm 0
\end{bmatrix}
\] | [83] |
| Labradorite (triclinic)   | \[
\begin{bmatrix}
96.3 \pm 0.1 & 53.5 \pm 4.8 & 43.2 \pm 4.3 & 8.9 \pm 1.1 & -4.4 \pm 1.7 & -2.1 \pm 2.2 \\
164.8 \pm 5.8 & 29.0 \pm 2.2 & -5.2 \pm 1.3 & -5.9 \pm 1.8 & -3.4 \pm 1.3 \\
150.5 \pm 10.5 & 7.2 \pm 1.3 & -5.2 \pm 1.3 & -9.4 \pm 0.6 & -2.4 \pm 2.3 \\
22.4 \pm 2.5 & -0.6 \pm 0.2 & -2.4 \pm 0.6 & -4.3 \pm 2.5 & -37.4 \pm 0.1 \\
32.3 \pm 2.6 & -0.6 \pm 0.2 & -2.4 \pm 0.6 & -4.3 \pm 2.5 & -37.4 \pm 0.1
\end{bmatrix}
\] | [55, 57, 59, 92] |
| Phases                  | Stiffness tensor mean $^{\text{min}}_{\text{std}}$ | References |
|-------------------------|--------------------------------------------------|------------|
| Lizardite (trigonal)    | \[
\begin{bmatrix}
232.7^{(2)}_{\pm 4.1} & 87.5^{(2)}_{\pm 4.1} & 19.3^{(2)}_{\pm 8.1} & 3.6^{(2)}_{\pm 1.4} & 0 & 0 \\
19.3^{(2)}_{\pm 8.1} & -3.6^{(2)}_{\pm 1.4} & 0 & 0 & 0 \\
82^{(2)}_{\pm 5.4} & 16.8^{(2)}_{\pm 8.8} & 0 & 0 & 0 \\
16.8^{(2)}_{\pm 8.8} & 3.6^{(2)}_{\pm 1.4} & 0 & 0 & 0 \\
\end{bmatrix}
\] | [93, 94] |
| Magnesite (hexagonal)  | \[
\begin{bmatrix}
260.4^{(2)}_{\pm 2.3} & 75.5^{(2)}_{\pm 1.6} & 59.9^{(2)}_{\pm 1.6} & 0 & 0 & 0 \\
59.9^{(2)}_{\pm 1.6} & 0 & 0 & 0 & 0 \\
156.3^{(2)}_{\pm 1.1} & 0 & 0 & 0 & 0 \\
56.6^{(2)}_{\pm 2.5} & 0 & 0 & 0 & 0 \\
92.4^{(0)}_{\pm 1.2} & 0 & 0 & 0 & 0 \\
\end{bmatrix}
\] | [61, 95] |
| Magnetite (cubic)      | \[
\begin{bmatrix}
270.9^{(3)}_{\pm 3.8} & 105.9^{(3)}_{\pm 2.2} & 105.9^{(3)}_{\pm 2.2} & 0 & 0 & 0 \\
105.9^{(3)}_{\pm 2.2} & 0 & 0 & 0 & 0 \\
270.9^{(3)}_{\pm 3.8} & 0 & 0 & 0 & 0 \\
96.5^{(3)}_{\pm 1.9} & 0 & 0 & 0 & 0 \\
96.5^{(3)}_{\pm 1.9} & 0 & 0 & 0 & 0 \\
\end{bmatrix}
\] | [83, 96] |
| Microcline (monoclinic)| \[
\begin{bmatrix}
66.4^{(1)}_{\pm 0} & 43.9^{(1)}_{\pm 0} & 25.9^{(1)}_{\pm 0} & 0 & 0 & -3.3^{(1)}_{\pm 0} \\
171^{(1)}_{\pm 0} & 19.2^{(1)}_{\pm 0} & 0 & 0 & -14.8^{(1)}_{\pm 0} & -13.1^{(1)}_{\pm 0} \\
121.5^{(1)}_{\pm 0} & 0 & 0 & 0 & 0 & 23.8^{(1)}_{\pm 0} \\
\end{bmatrix}
\] | [92] |
| Muscovite (monoclinic) | \[
\begin{bmatrix}
180.1^{(3)}_{\pm 2.3} & 35.3^{(3)}_{\pm 2.2} & 17.6^{(3)}_{\pm 4.5} & 0 & 0 & -2^{(1)}_{\pm 0} \\
178.2^{(2)}_{\pm 0.3} & 18.1^{(2)}_{\pm 1.3} & 0 & 0 & 3.9^{(1)}_{\pm 0} & 1.2^{(1)}_{\pm 0} \\
56.3^{(3)}_{\pm 2.4} & 0 & 0 & 0 & 0 & 69.3^{(3)}_{\pm 2.3} \\
\end{bmatrix}
\] | [59, 64, 97] |
| Phases               | Stiffness tensor mean $^{\mu \text{mm}}_{\mu \text{std.}}$ | References  |
|----------------------|-------------------------------------------------------------|-------------|
| Nepheline (hexagonal)| $\begin{bmatrix} 79.7^{(4)}_{\pm 3.5} & 40.5^{(4)}_{\pm 1.7} & 18.4^{(4)}_{\pm 3.4} & 0 & 0 & 0 \\ 79.7^{(4)}_{\pm 3.5} & 18.4^{(4)}_{\pm 3.4} & 0 & 0 & 0 \\ 128.6^{(4)}_{\pm 4.4} & 36^{(4)}_{\pm 1.1} & 0 & 0 \\ 36^{(4)}_{\pm 1.1} & 0 & 0 & 0 \\ 0 & 19.6^{(0)}_{\pm 0.9} \end{bmatrix}$ | $[59, 83, 98]$ |
| Obsidian (isotropic)| $\begin{bmatrix} 76.5^{(1)}_{\pm 0} & 19.5^{(1)}_{\pm 0} & 19.5^{(1)}_{\pm 0} & 0 & 0 & 0 \\ 76.5^{(1)}_{\pm 0} & 19.5^{(1)}_{\pm 0} & 0 & 0 & 0 \\ 76.5^{(1)}_{\pm 0} & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 \\ 28.5^{(0)}_{\pm 0} & 0 & 0 & 0 & 0 \\ 28.5^{(0)}_{\pm 0} & 0 & 0 & 0 & 0 \\ 28.5^{(0)}_{\pm 0} & 0 & 0 & 0 & 0 \end{bmatrix}$ | $[99]$ |
| Oligoclase (triclinic)| $\begin{bmatrix} 83.4^{(6)}_{\pm 2.3} & 40.8^{(6)}_{\pm 2.2} & 42^{(6)}_{\pm 5.8} & 6.1^{(1)}_{\pm 0} & -8.5^{(6)}_{\pm 4.9} & -0.6^{(4)}_{\pm 0} \\ 154.8^{(6)}_{\pm 11.8} & 30.6^{(6)}_{\pm 8.2} & -5.9^{(1)}_{\pm 0} & -9^{(6)}_{\pm 7.4} & -6.5^{(4)}_{\pm 0} \\ 136.8^{(6)}_{\pm 14.7} & -2.9^{(1)}_{\pm 0} & -12.7^{(6)}_{\pm 9.8} & -10.7^{(4)}_{\pm 0} \\ 19.1^{(6)}_{\pm 1.9} & -1.3^{(1)}_{\pm 0} & -1.7^{(6)}_{\pm 1.7} & -30.2^{(6)}_{\pm 1.8} & 0.8^{(1)}_{\pm 0} \\ 34.7^{(6)}_{\pm 0.9} & 0 & 0 & 0 & 0 \end{bmatrix}$ | $[57–59]$ |
| Orthoclase (monoclinic)| $\begin{bmatrix} 66.6^{(4)}_{\pm 10.3} & 37^{(4)}_{\pm 2.7} & 35.4^{(4)}_{\pm 12.3} & 0 & 0 & -10.9^{(4)}_{\pm 7.1} \\ 161.0^{(4)}_{\pm 14.5} & 22.4^{(4)}_{\pm 7} & 0 & 0 & -15.7^{(4)}_{\pm 6.6} \\ 125.1^{(4)}_{\pm 24.8} & 0 & 0 & 0 & -4.4^{(5)}_{\pm 10.1} \\ 16.4^{(4)}_{\pm 4.2} & -4.1^{(4)}_{\pm 5.1} & 0 & 0 & 0 \\ 34.2^{(4)}_{\pm 1.1} & 0 & 0 & 0 & 0 \\ 22.1^{(4)}_{\pm 3.8} \end{bmatrix}$ | $[59, 61, 100]$ |
| Periclase (cubic)| $\begin{bmatrix} 297^{(8)}_{\pm 1.5} & 95.4^{(8)}_{\pm 1.3} & 95.4^{(8)}_{\pm 1.3} & 0 & 0 & 0 \\ 297^{(8)}_{\pm 1.5} & 95.4^{(8)}_{\pm 1.3} & 0 & 0 & 0 \\ 297^{(8)}_{\pm 1.5} & 0 & 0 & 0 & 0 \\ 156.1^{(8)}_{\pm 0.4} & 0 & 0 & 0 & 0 \\ 156.1^{(8)}_{\pm 0.4} & 0 & 0 & 0 & 0 \\ 156.1^{(8)}_{\pm 0.4} \end{bmatrix}$ | $[101–108]$ |
Table 3 continued

| Phases                     | Stiffness tensor mean\(^{\min}_{\pm \text{std}}\) | References |
|----------------------------|-----------------------------------------------|------------|
| Phlogopite (monoclinic)    | \[
\begin{bmatrix}
179.1^{(2)}_{\pm1.3} & 31.9^{(2)}_{\pm1.6} & 17.2^{(4)}_{\pm0.6} & 0 & 0 & -6.9^{(2)}_{\pm12.9} \\
179.9^{(4)}_{\pm3.5} & 25.2^{(2)}_{\pm18.7} & 0 & 0 & -14^{(2)}_{\pm12.7} \\
54.9^{(3)}_{\pm6.2} & 8.7^{(3)}_{\pm4.6} & 0 & 0 & -3.9^{(3)}_{\pm4.2} \\
\end{bmatrix}
\] | [64, 109, 110] |
| Pyrope (cubic)             | \[
\begin{bmatrix}
293.3^{(3)}_{\pm5.1} & 108.2^{(3)}_{\pm3} & 108.2^{(3)}_{\pm3} & 0 & 0 & 0 \\
293.3^{(3)}_{\pm5.1} & 108.2^{(3)}_{\pm3} & 0 & 0 & 0 \\
293.3^{(3)}_{\pm5.1} & 0 & 0 & 0 & 0 \\
91.6^{(3)}_{\pm0} & 0 & 0 & 0 & 0 \\
91.6^{(3)}_{\pm0} & 0 & 0 & 0 & 0 \\
91.6^{(3)}_{\pm0} & 0 & 0 & 0 & 0 \\
\end{bmatrix}
\] | [83, 111, 112] |
| Rutile (tetragonal)        | \[
\begin{bmatrix}
269.2^{(4)}_{\pm1.9} & 177.6^{(4)}_{\pm1.4} & 147.9^{(4)}_{\pm1.4} & 0 & 0 & 0 \\
269.2^{(4)}_{\pm1.9} & 177.6^{(4)}_{\pm1.4} & 0 & 0 & 0 \\
482.2^{(4)}_{\pm2.4} & 123.9^{(4)}_{\pm0.5} & 0 & 0 & 0 \\
123.9^{(4)}_{\pm0.5} & 0 & 0 & 0 & 0 \\
\end{bmatrix}
\] | [113–116] |
| Sanidine (monoclinic)      | \[
\begin{bmatrix}
68.1^{(3)}_{\pm1.5} & 43^{(3)}_{\pm1.2} & 25.5^{(4)}_{\pm1} & 0 & 0 & -1.5^{(3)}_{\pm2.5} \\
174.7^{(3)}_{\pm3.2} & 18.2^{(3)}_{\pm3.5} & 0 & 0 & -12.3^{(3)}_{\pm2.7} \\
147.4^{(3)}_{\pm2.4} & 0 & 0 & 0 & 0.4^{(3)}_{\pm11.7} \\
17.6^{(3)}_{\pm2.9} & -7.9^{(3)}_{\pm5.6} & 0 & 0 & 34.3^{(3)}_{\pm1.5} \\
\end{bmatrix}
\] | [92, 100, 117] |
| Siderite (hexagonal)       | \[
\begin{bmatrix}
229^{(1)}_{\pm0} & 75.5^{(1)}_{\pm0} & 75^{(1)}_{\pm0} & 0 & 0 & 0 \\
229^{(1)}_{\pm0} & 75^{(1)}_{\pm0} & 0 & 0 & 0 \\
125^{(1)}_{\pm0} & 0 & 0 & 0 & 0 \\
41^{(1)}_{\pm0} & 0 & 0 & 0 & 0 \\
\end{bmatrix}
\] | [95] |

References:

[64, 109, 110, 83, 111, 112, 92, 100, 117, 113–116, 95]
P_{44}/P_0 = 8(-(1 + v)\rho^2 + v - 2)\alpha + 8(v\rho^2 + 1 - v) \tag{26}

with:

\[
P_0 = \frac{1 + v}{8E(1 - v)(1 - \rho^2)} \tag{27}
\]

\[
\alpha = \frac{\rho \arccos \rho - \rho\sqrt{1 - \rho^2}}{(1 - \rho^2)^{3/2}} \tag{28}
\]

**Elastic tensors of rock-forming minerals**

Table 3 summarizes the stiffness tensor data of the main rock-forming pristine minerals found in common rocks and used for this study. For each elastic constant, the mean value, the standard deviation, and the number of data available (in parenthesis) are provided. These data have either been obtained using experimental means (e.g., resonant frequency) or first principle–based simulations.

**Irradiated rocks composition**

The term *felsic aggregates* refers to igneous aggregates that contain relatively high amounts of quartz and feldspars, with mafic mineral content < 90% and light chemical elements such as silicon, aluminum, sodium, and potassium, resulting in a light color and a specific gravity under 3. The 21 tested felsic rocks are subdivided as follows:

- Seven gabbros, including two gabbros (# 14–15), a gabbro-porphyry (# 16), two diabase (# 17–18), a poikilitic diabase (# 19), and a basalt (# 20). The mineral compositions of these rocks are very similar (rich in plagioclase and low in quartz, P-corner of the double-triangle diagram). They contain a fraction of pyroxenes such as augite.
| No. | Agg. name | SiO₂ (%) | Class | IUGS classification | Mafic minerals (Q (%) | A (%) | P (%) | F (%) | Hbl (%) | Px (%) | Opx (%) | Cpx (%) | Ol (%) | Class |
|-----|-----------|----------|-------|---------------------|-----------------------|-------|-------|-------|---------|--------|---------|---------|-------|-------|
| 1   | Granite   | 72.2     | Acid  | Q (%)               | 25                   | 50    | 24    | 0     | 0       | 0      | 0       | 0       | 0     | Synep-granite |
| 2   | Granite   | 71.4     | Acid  | A (%)               | 30                   | 35    | 20    | 0     | 10      | 0      | 0       | 0       | 0     | Monzo-granite  |
| 3   | Granite   | 71.2     | Acid  | P (%)               | 30                   | 40    | 25    | 0     | 0       | 0      | 0       | 0       | 0     | Monzo-granite  |
| 4   | Porphyry granite | 75.5 | Ultra-acid | Q (%) | 40 | 30 | 15 | 0 | 0 | 0 | 0 | 0 | Syeno-granite |
| 5   | Granodiorite | 64.1 | Intermediate | A (%) | 20 | 10 | 40 | 0 | 15 | 0 | 0 | 0 | 0 | Granodiorite |
| 6   | Granodiorite | 66.2 | Acid | P (%)               | 20                   | 20    | 40    | 0     | 10      | 0      | 0       | 0       | 0     | Granodiorite  |
| 7   | Aphanitic liparite | 76.1 | Ultra-acid | A (%) | 35 | 33 | 32 | 0 | 0 | 0 | 0 | 0 | 0 | Monzo-granite  |
| 8   | Quartzitic andesite | 72.7 | Acid | Q (%)               | 30                   | 0     | 60    | 0     | 0       | 0      | 10      | 10      | 0     | Tonalite |
| 9   | Diorite    | 51.8     | Basic | Q (%)               | 5                   | 0     | 55    | 0     | 0       | 0      | 0       | 0       | 0     | Quartz diorite |
| 10  | Albitite   | 64.7     | Intermediate | A (%) | 0 | 0 | 70 | 30 | 0 | 0 | 0 | 0 | 0 | Albitite |
| 11  | Labradorite | 49.3 | Basic | Q (%)               | 0                   | 0     | 75    | 0     | 0       | 15      | 15      | 0       | 0     | Diorite |
| 12  | Urite      | 42.5     | Basic | A (%)               | 0                   | 0     | 0     | 85    | 0       | 10      | 10      | 0       | 0     | Urite |
| 13  | Gabbro     | 52.0     | Intermediate | A (%) | 0 | 0 | 60 | 0 | 0 | 40 | 40 | 0 | 0 | Gabbro |
| 14  | Gabbro     | 56.7     | Intermediate | A (%) | 2 | 0 | 53 | 0 | 45 | 0 | 0 | 0 | 0 | Gabbro |
| 15  | Gabbro-porphyr | 56.5 | Intermediate | A (%) | 0 | 0 | 50 | 0 | 0 | 50 | 50 | 0 | 0 | Gabbro |
| 16  | Porous diabase | 51.5 | Basic | A (%)               | 0                   | 0     | 60    | 0     | 0       | 39      | 39      | 0       | 0     | Gabbro |
| 17  | Diabase    | 50.0     | Basic | A (%)               | 0                   | 0     | 50    | 0     | 0       | 40      | 20      | 20      | 0     | Gabbro |
| 18  | Poikilitic diabase | 45.8 | Basic | Q (%)               | 0                   | 0     | 45    | 0     | 20      | 0       | 0       | 0       | 30    | Gabbro |
| 19  | Basalt     | 38.9     | Ultrabasic | A (%) | 0 | 0 | 50 | 0 | 0 | 0 | 0 | 0 | 0 | Gabbro |
| 20  | Laminated aleurolite | 61.8 | Intermediate | A (%) | 30 | 65 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | Aleurolite |
| 21  | Sandstone  | 73.9     | Acid | A (%)               | 45                   | 45    | 0     | 0     | 0       | 0       | 0       | 0       | 0     | Sandstone |
| 22  | Pyroxenite | 48.2     | Basic | Q (%)               | 0                   | 0     | 0     | 10    | 0       | 0      | 0       | 40      | 40    | 50    | OL-Pyroxenea OL-Ptopyroxb |
| 23  | Peridotite | 40.4     | Basic | Q (%)               | 0                   | 0     | 0     | 0     | 0       | 0      | 0       | 15      | 15    | 0     | PX-Peridotitea Wehrliteb |
and enstatite (orthopyroxene), and a minor amount of olivine.

- Five granites, including syneo-granites (#1 and #4, 65-90% alkali feldspars content) and monzo-granites (# 2, 3, 7, 35-60% alkali feldspars content). Granites # 1–4 are composed of the same minerals (>20% quartz, alkali feldspars and a minor content of mafic minerals such as hornblende). The average grain size (a.g.s.) of granites # 1–4 ranges from medium to large except for the porphyry granite, which has a smaller grain size.

- Three diorites: quartzic diorite (# 10), albatite (# 11, foid diorite), and labradiorite (# 12), composed primarily of plagioclases, pyroxenes, feldpathoids, micas, and small amounts of quartz. The mineral grain size of diorites here is small for both # 10 and # 11, and large for # 12.

- Two granodiorites (# 5–6) of compositions comparable to those of granites except for a higher plagioclases content. Other minerals include hornblende, biotite, and augite.

- Tonalite–Quartzitic andesite was the only silicate–felsic aggregate that was classified as tonalite. This class of rocks generally contains more than 20% quartz, plagioclases (mostly oligoclase and andesine), minor amounts of mafic minerals such as biotite, hornblende, or pyroxene, and usually <10% of alkali feldspars. The mineral grain size of tonalite is generally medium to fine.

- Large-grain urtite (# 13, 80–90% nepheline and minor content of pyroxenes such as aegirine or augite).

- Sandstone and laminated aleurolite were also classified with the other silicate-felsic aggregates here for the purpose of comparison. The mineral compositions of these two aggregates are very similar. The differences between sandstone and laminated aleurolite are that sandstone contains more quartz and less alkali feldspar than the laminated aleurolite. Moreover, laminated aleurolite contains a small amount of mica which was not clearly indicated in Denisov’s table [22]. The mineral grain size of sandstone is 0.3 mm, which is 10 times larger than laminated aleurolite.

Mafic aggregates are silicate aggregates that contain a large amount of mafic minerals (i.e., ≥ 90%) such as olivine, pyroxene, hornblende, etc. Mafic minerals are rich with iron and magnesium. Therefore, they are...
Table 5: Mineral composition of aggregates

| No. | Name                              | Composition                  | Density (g cm\(^{-3}\)) | Average grain size (mm) |
|-----|-----------------------------------|------------------------------|--------------------------|-------------------------|
| 1   | Large-grain granite               | Quartz: 25%                 | 2.59                     | 5                       |
|     |                                   | Microcline: 50%             |                          |                         |
|     |                                   | Oligoclase: 24%             |                          |                         |
|     |                                   | Biotite: 1%                 |                          |                         |
| 2   | Medium-grain granite              | Quartz: 30%                 | 2.65                     | 4                       |
|     |                                   | Microcline: 35%             |                          |                         |
|     |                                   | Oligoclase: 20%             |                          |                         |
|     |                                   | Biotite: 5%                 |                          |                         |
|     |                                   | Hornblende: 10%             |                          |                         |
| 3   | Medium-grain granite              | Quartz: 30%                 | 2.62                     | 2                       |
|     |                                   | Microcline: 40%             |                          |                         |
|     |                                   | Oligoclase: 25%             |                          |                         |
|     |                                   | Metallic oxide: 5%          |                          |                         |
| 4   | Small-grain porphyry granite      | Quartz: 40%                 | 2.57                     | 0.5                     |
|     |                                   | Microcline: 30%             |                          |                         |
|     |                                   | Oligoclase: 15%             |                          |                         |
|     |                                   | Muscovite: 15%              |                          |                         |
| 5   | Medium-grain granodiorite         | Quartz: 20%                 | 2.68                     | 2                       |
|     |                                   | Microcline: 10%             |                          |                         |
|     |                                   | Oligoclase: 40%             |                          |                         |
|     |                                   | Hornblende: 15%             |                          |                         |
|     |                                   | Niotite: 15%                |                          |                         |
| 6   | Medium-grain granodiorite         | Quartz: 20%                 | 2.76                     | 3                       |
|     |                                   | Microcline: 20%             |                          |                         |
|     |                                   | Oligoclase: 40%             |                          |                         |
|     |                                   | Biotite: 10%                |                          |                         |
|     |                                   | Hornblende: 10%             |                          |                         |
| 7   | Mphanitic liparite                | Quartz: 35%                 | 2.64                     | 0.5                     |
|     |                                   | Microcline: 33%             |                          |                         |
|     |                                   | Oligoclase: 32%             |                          |                         |
| 8   | Obsidian                          | Obsidian: 100%              | 2.3                      | 0                       |
| 9   | Fine-grain quartzitic andesite    | Quartz: 30%                 | 2.7                      | 0.3                     |
|     |                                   | Oligoclase: 60%             |                          |                         |
|     |                                   | Diopside: 10%               |                          |                         |
| 10  | Small-grain diorite               | Quartz: 5%                  | 2.73                     | 1.5                     |
|     |                                   | Oligoclase: 55%             |                          |                         |
|     |                                   | Mica: 30%                   |                          |                         |
|     |                                   | Metallic oxide: 10%         |                          |                         |
| 11  | Small-grain albitite              | Albite: 70%                 | 2.5                      | 1                       |
|     |                                   | Analcime: 30%               |                          |                         |
| 12  | Large-grain labradorite           | Labradorite: 75%            | 2.8                      | 5                       |
|     |                                   | Diopside: 15%               |                          |                         |
|     |                                   | Biotite: 5%                 |                          |                         |
|     |                                   | Magnetite: 5%               |                          |                         |
| 13  | Large-grain urtite (nephelinic syenite) | Nepheline: 85%             | 2.83                     | 5                       |
|     |                                   | Diopside: 10%               |                          |                         |
|     |                                   | Apatite: 5%                 |                          |                         |
| 14  | Medium-grain gabbro               | Labradorite: 60%            | 2.97                     | 2                       |
|     |                                   | Diopside: 40%               |                          |                         |
### Table 5 continued

| No. | Name                        | Composition                  | Density (g cm\(^{-3}\)) | Average grain size (mm) |
|-----|-----------------------------|------------------------------|--------------------------|-------------------------|
| 15  | Small-grain gabbro          | Oligoclase: 53%              | 2.68                     | 1                       |
|     |                             | Quartz: 2%                   |                          |                          |
|     |                             | Hornblende: 45%              |                          |                          |
| 16  | Gabbro-porphyry             | Oligoclase: 50%              | 2.65                     | 0.3                     |
|     |                             | Diopside: 50%                |                          |                          |
| 17  | Fine-grain porous diabase   | Labradorite: 60%             | 2.54                     | 0.3                     |
|     |                             | Diopside: 39%                |                          |                          |
|     |                             | Metallicoxide: 1%            |                          |                          |
| 18  | Fine-grain diabase          | Labradorite: 50%             | 2.92                     | 0.2                     |
|     |                             | Augite: 20%                  |                          |                          |
|     |                             | Enstatite: 20%               |                          |                          |
|     |                             | Chlorite: 10%                |                          |                          |
| 19  | Small-grain poikilitic diabase | Labradorite: 45%             | 2.76                     | 0.2                     |
|     |                             | Olivine: 30%                 |                          |                          |
|     |                             | Hornblende: 20%              |                          |                          |
|     |                             | Magnetite: 5%                |                          |                          |
| 20  | Fine-grain basalt           | Labradorite: 50%             | 2.76                     | 0.1                     |
|     |                             | Olivine: 30%                 |                          |                          |
|     |                             | Metallicoxide: 10%           |                          |                          |
|     |                             | Silica: 10%                  |                          |                          |
| 21  | Small-grain pyroxenite      | Olivine: 50%                 | 3                        | 0.1                     |
|     |                             | Plagioclase: 10%             |                          |                          |
|     |                             | Enstatite: 40%               |                          |                          |
| 22  | Medium-grain peridotite     | Olivine: 80%                 | 3.3                      | 2                       |
|     |                             | Diopside: 15%                |                          |                          |
|     |                             | Metallicoxide: 5%            |                          |                          |
| 23  | Medium-grain olivinite      | Olivine: 95%                 | 3.37                     | 3                       |
|     |                             | Metallicoxide: 5%            |                          |                          |
| 24  | Fine-grain serpentinized dunite | Olivine: 80%                 | 3                        | 0.3                     |
|     |                             | Serpentine: 10%              |                          |                          |
|     |                             | Enstatite: 10%               |                          |                          |
| 25  | Fine-grain serpentinized dunite | Olivine: 60%                 | 2.97                     | 0.01                    |
|     |                             | Serpentine: 40%              |                          |                          |
| 26  | Fine-grain serpentinized dunite | Olivine: 25%                 | 2.6                      | 0.03                    |
|     |                             | Serpentine: 75%              |                          |                          |
| 27  | Medium-grain hornblendite   | Hornblende: 100%             | 2.3                      | 0.2                     |
| 28  | Fine-grain laminated aleurolite | Quartz: 25.5%               | 2.3                      | 0.03                    |
|     |                             | Feldspar: 55.25%             |                          |                          |
|     |                             | Mica: 2.125%                 |                          |                          |
|     |                             | Metallicoxide: 2.125%        |                          |                          |
|     |                             | Porosity: 15%                |                          |                          |
| 29  | Small-grain sandstone       | Quartz: 45%                  | 2.54                     | 0.3                     |
|     |                             | Feldspar: 45%                |                          |                          |
|     |                             | Metallicoxide: 10%           |                          |                          |
| 30  | Fine-grain limestone        | Calcite: 84%                 | 2.27                     | 0.1                     |
|     |                             | Porosity: 16%                |                          |                          |
| 31  | Small-grain limestone       | Calcite: 100%                | – 1                      | 0.5                     |
dark in color and heavy in weight. Some mafic aggregates contain a minor amount of plagioclases. From this classification, six irradiated silicate aggregates fall into this classification. These include:

- Dunite: Two irradiated silicate-mafic aggregates can be classified as dunite. These two aggregates are olivinite No. 23 and dunite No. 24. Dunite is usually rich with olivine mineral and contains minor amounts of clinopyroxene, orthopyroxene, spinel, and magnetite. Dunite No. 24 contains a small amount (10%) of orthopyroxene, 10% of serpentine, and the remainder is olivine, with fine grain size, while olivinite No. 23 contains mostly olivine and 5% of ore minerals, with a medium grain size.

- OL-Pyroxene: Pyroxenite irradiated silicate-mafic aggregate (No. 21) was classified in this work. This aggregate contains 50% of olivine mineral and 40% pyroxene (i.e., 40% clinopyroxene [enstatite]), and a minor amount of plagioclases (10%). The size of mineral grain of pyroxenite is 0.1 mm (fine).

- Periodotite: (No. 22, 80% olivine, 15% orthopyroxene (15%), a.g.s.: 2 mm).

- Hornblendite: (No. 27, 100% hornblende, a.g.s.: 2 mm).

The remaining rock samples (# 30–35) are classified as carbonates, including two high-calcite limestones (# 30–31) and a dolimitic limestone (32: 20% dolomite), all of relatively fine grain structures <0.5 mm. The other three irradiated sedimentary carbonates correspond to a porous fine magnesite (# 33, 99% magnesite 0.05 mm), a porous fine siderite (# 34) with a quartz content of 10 (a.g.s.: 0.04 mm), and dolomite (# 35) containing 5% siderite (a.g.s.: 2 mm).

While Table 4 is limited to silicate-bearing rocks and provides the necessary data to create Figs. 1, 2 and Table 5 provides the mineral contents of all the aggregates used to complete this study.

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