Enhanced Group Sparse Beamforming for Green Cloud-RAN: A Random Matrix Approach

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Abstract—Group sparse beamforming is a general framework to minimize the network power consumption for cloud radio access networks, which, however, suffers high computational complexity. In particular, a complex optimization problem needs to be solved to obtain the remote radio head (RRH) ordering criterion in each transmission block, which will help to determine the active RRHs and the associated fronthaul links. In this paper, we propose innovative approaches to reduce the complexity of this key step in group sparse beamforming. Specifically, we first develop a smoothed $\ell_p$-minimization approach with the iterative reweighted-$\ell_2$ algorithm to return a Karush–Kuhn–Tucker (KKT) point solution, as well as enhance the capability of inducing group sparsity in the beamforming vectors. By leveraging the Lagrangian duality theory, we obtain closed-form solutions at each iteration to reduce the computational complexity. The well-structured solutions provide opportunities to apply the large-dimensional random matrix theory to derive deterministic approximations for the RRH ordering criterion. Such an approach helps to guide the RRH selection only based on the statistical channel state information, which does not require frequent update, thereby significantly reducing the computation overhead. Simulation results shall demonstrate the performance gains of the proposed $\ell_p$-minimization approach, as well as the effectiveness of the large system analysis-based framework for computing the RRH ordering criterion.

Index Terms—Cloud-RAN, green communications, sparse optimization, smoothed $\ell_p$-minimization, Lagrangian duality, and random matrix theory.

I. INTRODUCTION

NETWORK densification [2]–[4] has been proposed as a promising way to provide ultra-high data rates, achieve low latency, and support ubiquitous connectivity for the upcoming 5G networks [5]. However, to fully harness the benefits of dense wireless networks, formidable challenges arise, including interference management, radio resource allocation, mobility management, as well as high capital expenditure and operating expenditure. Cloud-RAN emerges as a disruptive technology to deploy cost-effective dense wireless networks [6], [7]. It can significantly improve both energy and spectral efficiency, by leveraging recent advances in cloud computing and network function virtualization [8]. With shared computation resources at the cloud data center and distributed low-cost low-power remote radio heads (RRHs), Cloud-RAN provides an ideal platform to achieve the benefits of network cooperation and coordination [9]. There is a unique characteristic in Cloud-RANs, namely, the high-capacity fronthaul links are required to connect the cloud center and RRHs [10], [11]. Such links will consume power comparable to that of each RRH, and thus brings new challenges to design green Cloud-RANs. To address this issue, a new performance metric, i.e., the network power consumption, which consists of both the fronthaul link power consumption and RRH transmit power consumption, has been identified in [7] for the green Cloud-RAN design.

Unfortunately, the network power minimization problem turns out to be a mixed-integer nonlinear programming problem [12], which is highly intractable. Specifically, the combinatorial composite objective function involves a discrete component, indicating which RRHs and the corresponding fronthaul links should be switched on, and a continuous component, i.e., beamformers to reduce RRH transmit power. To address this challenge, a unique group sparsity structure in the optimal beamforming vector has been identified in [7] to unify RRH selection and beamformer optimization. Accordingly, a novel three-stage group sparse beamforming framework was proposed to promote group sparsity in the solution. Specifically, a mixed $\ell_1/\ell_2$-minimization approach was first proposed to induce group sparsity in the solution, thereby guiding the RRH selection via solving a sequence of convex feasibility problems, followed by coordinated beamforming to minimize the transmit power for the active RRHs.

Although the group sparse beamforming framework provides polynomial-time complexity algorithms via convex
optimization, it has the limited capability to enhance group sparsity compared to the non-convex approaches [13], [14]. In particular, the smoothed $\ell_p$-minimization supported by the iterative reweighted-$\ell_2$ algorithm was developed in [15] to enhance sparsity for multicast group sparse beamforming. However, the computation burden of this iterative algorithm is still prohibitive in dense wireless networks with a large number of RRHs and mobile users. In [16], a generic two-stage approach was proposed to solve large-scale convex optimization problems in dense wireless cooperative networks via matrix stuffing and operator splitting, i.e., the alternating direction method of multipliers (ADMM) [17], [18]. This approach also enables parallel computing and infeasibility detection. However, as the proposed solutions need to be accomplished for each channel realization, and also due to the iterative procedures of the group sparse beamforming framework, it is still computationally expensive.

In this paper, we improve the performance of group sparse beamforming [7] via $\ell_p$-minimization, and a special emphasis is on reducing the computational complexity, with two ingredients: closed-form solutions for each iteration, and the deterministic equivalents of the optimal Lagrange multipliers. Specifically, we first develop an iterative reweighted-$\ell_2$ algorithm with closed-form solutions at each iteration via leveraging the principles of the majorization-minimization (MM) algorithm [19] and the Lagrangian duality theory [20]. It turns out that the proposed iterative reweighted-$\ell_2$ algorithm can find a KKT point for the smoothed non-convex $\ell_p$-minimization problem. Furthermore, this reveals the explicit structures of the optimal solutions to each subproblem in the iterative reweighted-$\ell_2$ algorithm, while the convex optimization approach in [7], [15], and [21] fails to obtain the closed-form solutions. Thereafter, the well-structured closed-form solutions provide opportunities to leverage the large-dimensional random matrix theory [22]–[24] to perform the asymptotic analysis in the large system regimes [25], [26]. Specifically, the deterministic equivalents of the optimal Lagrange multipliers are derived based on the recent results of large random matrix analysis [27] to decouple the dependency of system parameters. These results are further used to perform an asymptotic analysis for computing the RRH ordering criterion, which only depends on long-term channel attenuation, thereby significantly reducing the computation overhead compared with previous algorithms that heavily depends on instantaneous CSI [7], [15], [21], [28]–[31].

Based on the above proposal, we provide a three-stage enhanced group sparse beamforming framework for green Cloud-RAN via random matrix theory. Specifically, in the first stage, we compute the enhanced RRH ordering criterion only based on the statistical CSI. This thus avoids frequent updates, thereby significantly reducing computational complexity, which is a sharp difference compared to the original proposal in [8]. This new algorithm is based on the principles of the MM algorithm and the Lagrangian duality theory, followed by the random matrix theory. With the obtained deterministic equivalents of RRH ordering criterion, a two-stage large-scale convex optimization framework [16] is adopted to solve a sequence of convex feasibility problems to determine the active RRHs in the second stage, as well as solving the transmit power minimization problem for the active RRHs in the final stage. Note that global instantaneous CSI is required for these two stages. Simulation results are provided to demonstrate the improvement of the enhanced group sparse beamforming framework. Moreover, the deterministic approximations turn out to be accurate even in the finite-sized systems.

### A. Related Works

1) **Sparse Optimization in Wireless Networks:** The sparse optimization paradigm has recently been popular for complicated network optimization problems in wireless network design, e.g., the group sparse beamforming framework for green Cloud-RAN design [7], [15], [30]–[32], wireless caching networks [33], [34], user admission control [15], [35], as well as computation offloading [36]. In particular, the convex relaxation approach provides a principled way to induce sparsity via the $\ell_1$-minimization [35] for individual sparsity inducing and the mixed $\ell_1/\ell_2$-minimization for group sparsity inducing [7]. The reweighted-$\ell_1$ algorithm [13] and the reweighted-$\ell_2$ algorithm [15] were further developed to enhance sparsity. To enable parallel and distributed computing, the first-order method ADMM algorithm was adopted to solve the group sparse beamforming problems [37]. A generic large-scale convex optimization framework was further proposed to solve general large-scale convex programs in dense wireless networks to enable scalability, parallel computing and infeasibility detection [16].

However, all the above algorithms need to be computed for each channel realization, which is computationally expensive. In this paper, we adopt large system analysis to compute the RRH ordering criterion for network adaptation only based on statistical CSI.

2) **Large System Analysis via Random Matrix Theory:** Random matrix theory [22] has been proven powerful for performance analysis, and the understanding and improving algorithms in wireless communications [23], [38], signal processing [39], and machine learning [40], [41], especially in large dimensional regimes for applications in the era of big data [42]. In dense wireless networks, random matrix theory provides a powerful way for performance analysis and algorithm design. In particular, the large system analysis was performed for simple precoding schemes, e.g., regularized zero-forcing in MISO broadcast channels with imperfect CSI [24]. A random matrix approach to the optimal coordinated multicell beamforming for massive MIMO was presented in [43] without close-form expressions for the optimal Lagrange multipliers. A simple channel model with two cells under different coordination levels was considered in [25].

However, all of the above results cannot be directly applied in the group sparse beamforming framework in dense Cloud-RAN due to the general channel models with heterogeneous pathloss and the complicated beamformer structures with fully cooperative transmission. To determine the RRH ordering criterion based on statistical CSI, we adopt the technique in [26] and [27] to compute the closed-forms for the optimal Lagrange multipliers for each iteration in the procedure of reweighted-$\ell_2$ minimization for sparsity inducing.
**B. Organization**

The remainder of the paper is organized as follows. Section II presents the system model and problem formulation, followed by performance analysis with the proposed three-stage enhanced group sparse beamforming framework for green Cloud-RAN. In Section III, the iterative reweighted-$\ell_2$ algorithm for group sparse beamforming is presented via the principle of MM algorithm and duality theory. The large system analysis for RRH ordering is performed in Section IV. Simulation results will be demonstrated in Section V. Finally, conclusions and discussions are presented in Section VI. To keep the main text clean and free of technical details, we divert most of the proofs to the Appendix.

**Notations:** Throughout this paper, $\| \cdot \|_p$ stands for either the size of a set or the absolute value of a scalar, depending on the context. $\| M \|$ is the spectral radius of the Hermitian matrix $M$. Boldface lower case and upper case letters represent vectors and matrices, respectively. $(\cdot)^{-1}, (\cdot)^T, (\cdot)^H$ and $\text{Tr}(\cdot)$ denote the inverse, transpose, Hermitian and trace operators, respectively. We use $\mathbb{C}$ to represent complex domain. $\mathbb{E} [\cdot]$ denotes the expectation of a random variable. We denote $A = \text{diag}(x_1, \ldots, x_N)$ and $I_N$ as a diagonal matrix of order $N$ and the identity matrix of order $N$, respectively.

**II. SYSTEM MODEL AND PROBLEM FORMULATION**

**A. System Model**

Consider a Cloud-RAN with $L$ RRHs and $K$ single-antenna mobile users (MUs), where each RRH is equipped with $N$ antennas. In Cloud-RANs, the BU pool will perform the centralized signal processing and is connected to all the RRHs via high-capacity and low-latency fronthaul links. In this paper, we will focus on the downlink signal processing. Specifically, let $v_k \in \mathbb{C}^N$ be the transmit beamforming vector from the $l$-th RRH to the $k$-th MU. The received signal $y_k \in \mathbb{C}$ at MU $k$ is given by

$$y_k = \sum_{l=1}^{L} h_{lk}^H v_k s_k + \sum_{l \neq l} \sum_{i=1}^{L} h_{lk}^H v_l s_l + n_k,$$

where $h_{lk} \in \mathbb{C}^N$ is the channel propagation between MU $k$ and RRH $l$, $s_k \in \mathbb{C}$ with $\mathbb{E}[|s_k|^2] = 1$ is the encoded transmission information symbol for MU $k$, and $n_k \sim \mathcal{CN}(0, \sigma_k^2)$ is the additive Gaussian noise at MU $k$.

We assume that $s_k$’s and $n_k$’s are mutually independent and all the MUs apply single-user detection. The signal-to-interference-plus-noise ratio (SINR) for MU $k$ is given by

$$\text{SINR}_k = \frac{|h_{lk}^H v_k|^2}{\sum_{i \neq k} |h_{lk}^H v_i|^2 + \sigma_k^2},$$

where $h_k = [h_{1k}, \ldots, h_{Lk}]^T \in \mathbb{C}^{LN}$ is the vector consisting of the channel coefficients from all the RRHs to MU $k$, and $v_k = [v_{1k}, \ldots, v_{Lk}]^T \in \mathbb{C}^{LN}$ is the aggregate beamforming vector for the MU $k$ from all the RRHs.

**B. Problem Formulation**

In this paper, we aim at designing a green Cloud-RAN by minimizing the network power consumption, which consists of the fronthaul links power consumption, as well as the RRH transmit power consumption [7]. Specifically, let $v = [v_{lk}] \in \mathbb{C}^{KLN}$ be the aggregate beamforming vector from all the RRHs to all the MUs. Define the support of the beamforming vector $v$ as $T(v) = \{i | v_i \neq 0\}$, where $v = [v_i]$ is indexed by $i \in \mathcal{V}$ with $\mathcal{V} = \{1, \ldots, KLN\}$. The relative fronthaul network power consumption is given by

$$f_1(v) = \sum_{i=1}^{L} P_f^i |T(v) \cap V_i \neq \emptyset|,$$

where $P_f^i \geq 0$ is the relative fronthaul link power consumption [7] (i.e., the static power saving when both the fronthaul link and the corresponding RRH are switched off), $V_i = \{(l-1)KN + 1, \ldots, lKN\}$, $\forall l \in \mathcal{L}$, is a partition of $\mathcal{V}$, and $I(T \cap V_i \neq \emptyset)$ is an indicator function that takes value 1 if $T \cap V_i \neq \emptyset$ and 0 otherwise. Note that $f_1$ is a non-convex combinatorial function.

Furthermore, the total transmit power consumption is given by

$$f_2(v) = \sum_{i=1}^{L} \sum_{k=1}^{K} \frac{1}{\zeta_l} \|v_k\|_2^2,$$

where $\zeta > 0$ is the drain inefficiency coefficient of the radio frequency power amplifier [7]. Therefore, the network power consumption is represented by the combinatorial composite function

$$f(v) = f_1(v) + f_2(v).$$

Given the QoS thresholds $\gamma = (\gamma_1, \ldots, \gamma_K)$ for all the MUs, in this paper, we aim at solving the following network power consumption minimization problem with the QoS constraints:

$$\mathcal{B}: \text{minimize } f_1(v) + f_2(v)$$

subject to

$$\sum_{i \neq k} |h_{lk}^H v_i|^2 + \sigma_k^2 \geq \gamma_k, \forall k.$$

Let $\tilde{v}_i = [v_i|_{V_i}] = [v_{i1}, \ldots, v_{iK}]^T \in \mathbb{C}^{KN}$ form the beamforming coefficient group from RRH $l$ to all the MUs. Note that, when the RRH $l$ is switched off, all the beamforming coefficients in $\tilde{v}_i$ will be set to zeros simultaneously. Observing that there may be multiple RRHs being switched off to minimize the network power consumption, the optimal beamforming vector $v = [v_1^T, \ldots, v_K^T]^T \in \mathbb{C}^{KLN}$ should have a group-sparsity structure. Therefore, problem $\mathcal{B}$ is called a group sparse beamforming problem [7]. Note that, to simplify the presentation, we only impose the QoS constraints in problem $\mathcal{B}$. However, the proposed instantaneous CSI based iterative reweighted-$\ell_2$ algorithm can be extended to the scenario with per-RRH transmit power constraints, following the principles in [20]. More technical efforts are required to derive the asymptotic results using the random matrix method with more complicated structures of the optimal beamformers.
C. Problem Analysis

Although the constraints in problem $\mathcal{P}$ can be reformulated as convex second-order cone constraints, the non-convex objective function makes it highly intractable. To address this challenge, a weighted mixed $\ell_1/\ell_2$-norm minimization approach was proposed in [7] to convexify the objective and induce the group sparsity in beamforming vector $v$, thereby guiding the RRH ordering to enable adaptively RRH selection. Specifically, we will first solve the $\ell_1/\ell_2$-norm minimization problem, and denote $\tilde{v}_1^*, \ldots, \tilde{v}_L^*$ as the induced (approximated) group sparse beamforming vectors. Then the following RRH ordering criterion is adopted to determine which RRHs should be switched off [7]:

$$\theta_l = \kappa_l \|\tilde{v}_l^*\|_2^2, \quad \forall l = 1, \ldots, L,$$

(7)

where $\kappa_l = \sum_{k=1}^{K} \|h_{lk}\|_2^2/v_l$. In particular, the group sparsity structure information for beamforming vector $v$ is extracted from the squared $\ell_2$-norm of the beamforming vectors $\tilde{v}_l$'s, i.e., $\|\tilde{v}_1^*\|_2^2, \ldots, \|\tilde{v}_L^*\|_2^2$. The RRH with a smaller $\theta_l$ will have a higher priority to be switched off. Based on the RRH ordering result $\theta^*$ in (7), a bi-section search approach can be used to find the optimal active RRHs [7] via solving a sequence of the following feasibility problems:

$$\mathcal{F}(A[i]): \text{find } v_1, \ldots, v_K$$

subject to

$$\frac{|h_l^H v_k|^2}{\sum_{l \neq k} |h_l^H v_l|^2 + \sigma_k^2} \geq \gamma_k, \quad \forall k,$$

(8)

where $v_k = [v_{ik}] \in C^{|A[i]|}$ and $h_k = [h_{kl}] \in C^{|A[i]|}$. Problem $\mathcal{F}(A[i])$ turns out to be convex via reformulating the QoS constraints as second-order cone constraints [7]. To further enhance the sparsity as well as to seek the quadratic forms of the beamforming vectors in the multicast transmission setting, a smoothed $\ell_p$-minimization approach was proposed in [15]. To scale to large problem sizes in dense Cloud-RANs, a two-stage large-scale parallel convex optimization framework was developed in [16] with the capability of infeasibility detection.

However, all of the above developed algorithms bear high computation overhead. In particular, while the feasibility problem (8) for RRH selection can be efficiently solved with the large-scale optimization algorithm in [8], the RRH ordering criterion in (7) may be highly complicated to obtain, especially with the non-convex formulation as in [15]. Moreover, the ordering criterion needs to be recomputed for each transmission slot, and depends on instantaneous CSI. Observing that the statistical CSI normally changes much slower than the instantaneous CSI, to reduce the computational burden, we propose to compute the RRH ordering criterion (7) only based on statistical CSI, i.e., the long-term channel attenuation. This is achieved by first developing a group sparsity penalty with quadratic forms in the aggregative beamforming vector $v$, followed by an iterative reweighted-$\ell_2$ algorithm with closed-form solutions at each iteration via Lagrangian duality theory, as will be presented in Section III. Then asymptotic analysis is performed to obtain the RRH ordering criterion (7) based only on statistical CSI by leveraging the large-dimensional random matrix theory [23], [24], [27], as will be presented in Section IV.

Overall, the proposed three-stage enhanced group sparse beamforming framework is presented in Fig. 1. Specifically, in the first stage, the RRH ordering criterion $\theta^*$ is calculated only based on statistical CSI using Algorithm 2. In the second stage, the set of active RRHs $A^*$ is obtained based on instantaneous CSI via solving a sequence of convex feasibility problems $\mathcal{F}(A[i])$ using the large-scale convex optimization framework in [16]. In the third stage, the transmit power is minimized by solving the convex program (6) with the fixed active RRHs $A^*$ using the large-scale convex optimization algorithm in [16]. Overall, the proposed enhanced group sparse beamforming framework is scalable to large network sizes. This paper will focus on developing an effective algorithm for the first stage.

Remark 1: In this paper, we assume that, in the first stage, problem $\mathcal{P}$ (6) is feasible for developing Algorithm 1 and Algorithm 2 to determine the RRH ordering criterion based on the instantaneous CSI and statistical CSI, respectively. We enable the capability of handing the infeasibility in the second stage based on the instantaneous CSI, using the large-scale convex optimization algorithm [16]. Furthermore, when problem $\mathcal{F}$ (8) is infeasible with all RRHs active, we adopt the user admission algorithm to find the maximum number of admitted users [15].

III. GROUP SPARSE BEAMFORMING VIA ITERATIVE REWEIGHTED-$\ell_2$ ALGORITHM

In this section, we develop a group sparse beamforming approach based on the smoothed $\ell_p$-minimization, supported by an iterative reweighted-$\ell_2$ algorithm, thereby enhancing the group sparsity in the beamforming vectors. Instead of reformulating the QoS constraints in problem $\mathcal{P}$ as second-order cone constraints [7], we use the Lagrangian duality theory to reveal the structures of the optimal solutions at each iteration. The results will assist the large system analysis in Section IV.

A. Group Sparsity Inducing Optimization via Smoothed $\ell_p$-Minimization

To induce the group sparsity structure in the beamforming vector $v$, thereby guiding the RRH ordering, the weighted mixed $\ell_1/\ell_2$-norm was proposed in [7]. However, the non-smooth mixed $\ell_1/\ell_2$-norm fails to introduce the quadratic forms in the beamforming vector $v$, in order to be compatible with the quadratic QoS constraints so that the Lagrangian
duality theory can be applied [20]. To address this challenge, we adopt the following smoothed $\ell_p$-minimization ($0 < p \leq 1$) approach to induce group sparsity [14], [15]:

$$\mathcal{P}_{\text{GSBF}}: \min_{v} \ g_p(v; \epsilon) := \sum_{l=1}^{L} v_l \left( \| {\tilde{v}}_l \|_2^2 + \epsilon^2 \right)^{p/2}$$

subject to

$$\sum_{i \neq k} \| h_i^H v_k \|_2^2 + \sigma_k^2 \geq \gamma_k, \ \forall k,$$

where $\epsilon > 0$ is some fixed regularizing parameter and $v_l > 0$ is the weight for the beamforming coefficient group $v_l$ by encoding the prior information of system parameters [7]. Compared with the mixed $\ell_1/\ell_2$-norm minimization approach, the $\ell_p$-minimization approach can induce sparser solutions based on the fact $\| z \|_0 = \lim_{p \to 0} \| z \|_p^p = \lim_{p \to 0} \sum_j | z_j |^p$.

Unfortunately, problem (9) is non-convex due to the non-convexity of both the objective function and the QoS constraints.

B. Iterative Reweighted-$\ell_2$ Algorithm

We use the MM algorithm and the Lagrangian duality theory to solve problem (9) with closed-form solutions. Specifically, this approach generates the iterates $\{v^{[n]}\}$ by successively minimizing upper bounds $Q(v; v^{[n]})$ of the objective function $g_p(v; \epsilon)$. We adopt the following upper bounds to approximate the smoothed $\ell_p$-norm $g(v; \epsilon)$ by leveraging the results of the expectation-maximization (EM) algorithm [44].

Proposition 1: Given the value of $v^{[n]}$ at the $n$-th iteration, an upper bound for the objective function $g_p(v; \epsilon)$ can be constructed as follows:

$$Q(v; \omega^{[n]}) := \sum_{l=1}^{L} \omega_l^{[n]} \| {\tilde{v}}_l \|_2^2,$$

where

$$\omega_l^{[n]} = \frac{p v_l}{2} \left( \| v_l^{[n]} \|_2^2 + \epsilon^2 \right)^{\frac{p-1}{p}}, \ \forall l = 1, \ldots, L.$$

Proof: The proof is mostly based on [15, Proposition 1].

Therefore, at the $n$-th iteration, we need to solve the following optimization problem:

$$\mathcal{P}_{\text{GSBF}}^{[n]}: \min_{v} \sum_{l=1}^{L} \omega_l^{[n]} \| {\tilde{v}}_l \|_2^2$$

subject to

$$\sum_{i \neq k} \| h_i^H v_k \|_2^2 + \sigma_k^2 \geq \gamma_k, \ \forall k,$$

which is non-convex due to the non-convex QoS constraints.

Although the QoS constraints can be reformulated as second-order cone constraints as in [7], in this paper, we leverage the Lagrangian duality theory to obtain explicit structures of the optimal solution to problem $\mathcal{P}_{\text{GSBF}}^{[n]}$ thereby reducing the computational complexity and further aiding the large system analysis in next section. The success of applying the Lagrangian duality approach is based on the fact that strong duality holds for problem $\mathcal{P}_{\text{GSBF}}^{[n]}$ [45], i.e., the gap between the primal optimal objective and the dual optimal objective is zero.

1) Simple Solution Structures: As the strong duality holds for problem $\mathcal{P}_{\text{GSBF}}^{[n]}$, we solve it using duality theory. Specifically, let $\lambda_k/(NL) \geq 0$ denote the Lagrange multipliers corresponding to the QoS constraints in problem $\mathcal{P}_{\text{GSBF}}^{[n]}$.

Define the Lagrangian function $\mathcal{L}(v_k, \lambda)$ with $\lambda = \{\lambda_k\}$ as

$$\mathcal{L}(v_k, \lambda) := \sum_{k=1}^{K} \frac{\lambda_k}{LN} \left( \sum_{i \neq k} \| h_i^H v_k \|_2^2 + \sigma_k^2 - \frac{1}{\gamma_k} h_i^H v_k^2 \right) + \sum_{k=1}^{K} v_k^H Q^{[n]} v_k,$$

where $Q^{[n]} \in \mathbb{C}^{LN \times LN}$ is a block diagonal matrix with the scaled identity matrix $\omega_l^{[n]} v_l I_N$ as the $l$-th main diagonal block square matrix.

To find the optimal $v_k$’s, we take the gradient of the Lagrangian function $\mathcal{L}(v, \lambda)$ with respect to $v_k$ and set it to zero, which implies

$$Q^{[n]} v_k + \sum_{i \neq k} \frac{\lambda_{i}}{LN} h_i h_i^H v_k - \frac{\lambda_k}{LN} h_k h_k^H v_k = 0.$$

By adding $\frac{\lambda_k}{(NL)} h_k h_k^H v_k$ to both sides of (14), we have

$$(Q^{[n]} + \sum_{i=1}^{K} \frac{\lambda_i}{LN} h_i h_i^H) v_k = \frac{\lambda_k}{LN} \left( I + \frac{1}{\gamma_k} \right) h_k h_k^H v_k.$$

which implies $v_k = (Q^{[n]} + \sum_{i=1}^{K} \frac{\lambda_i}{(LN)} h_i h_i^H)^{-1} h_k h_k^H v_k$. As $(\lambda_k/(NL)) (I + 1/\gamma_k) h_k h_k^H$ is a scalar, the optimal $v_k$ must be parallel to the beamforming direction

$$\tilde{v}_k = \left( Q^{[n]} + \sum_{i=1}^{K} \frac{\lambda_i}{LN} h_i h_i^H \right)^{-1} h_k, \ \forall k.$$
Here, \([M]_{ij}\) denotes the \((i, j)\)-th element of the matrix \(M \in \mathbb{R}^{K \times K}\).

To find the optimal \(\lambda\)-parameter, by multiplying both sides by \(h_k^H\left(Q^n + \sum_{i=1}^{K} \frac{\lambda_i}{LN} h_i h_i^H\right)^{-1}\) in (15), we obtain \(h_k^H v_k\) as
\[
\frac{\lambda_k}{LN} \left(1 + \frac{1}{\gamma_k}\right) h_k^H \left(Q^n + \sum_{i=1}^{K} \frac{\lambda_i}{LN} h_i h_i^H\right)^{-1} h_k h_k^H v_k, \tag{20}
\]
which implies
\[
\lambda_k = LN \left[\left(1 + \frac{1}{\gamma_k}\right) h_k^H \left(Q^n + \sum_{i=1}^{K} \frac{\lambda_i}{LN} h_i h_i^H\right)^{-1} h_k\right]^{-1}. \tag{21}
\]
These fixed-point equations can be computed using iterative function evaluation.

Based on (17), (19) and (21), we obtain the squared \(\ell_2\)-norm of the optimal solution to problem \(P_{\text{GSBF}}^n\) as follows:
\[
\|\hat{v}_I^n\|_2^2 = \sum_{k=1}^{K} v_k^H Q_k v_k, \tag{22}
\]
where \(Q_k \in \mathbb{C}^{NL \times NL}\) is a block diagonal matrix with the identity matrix \(I_N\) as the \(l\)-th main diagonal block square matrix and zeros elsewhere. Note that the optimal powers \(p_k\)'s (19) and Lagrangian multipliers \(\lambda_k\)'s (21) should depend on the weights \(o_l^n\)'s (11) at each iteration \(n\).

The instantaneous CSI based iterative reweighted-\(\ell_2\) algorithm for group sparse beamforming is presented in Algorithm 1. We have the following result for its performance and convergence.

**Algorithm 1** Instantaneous CSI Based Iterative Reweighted-\(\ell_2\) Algorithm for Problem \(P_{\text{GSBF}}\)

**input:** Initialize \(o_l^{[0]} = (1, \ldots, 1); I\) (the maximum number of iterations)

Repeat
1) Compute the squared \(\ell_2\)-norm of the solution to problem \(P_{\text{GSBF}}^n\), \(\|\hat{v}_I^n\|_2^2, \ldots, \|\hat{v}_L^n\|_2^2\), using (17), (19), (21) and (22).
2) Update the weights \(o_l^{[n+1]}\) using (11).

Until convergence or attain the maximum iterations and return.

**output:** RRH ordering criterion \(\theta\) (7).

**Theorem 1:** Let \(\{\hat{v}_i^n\}_{n=1}^{\infty}\) be the sequence generated by the iterative reweighted-\(\ell_2\) algorithm. Then, every limit point \(\hat{v}\) of \(\{\hat{v}_i^n\}_{n=1}^{\infty}\) has the following properties:
1) \(\hat{v}\) is a KKT point of problem \(P_{\text{GSBF}}\) (9);
2) \(g_p(\hat{v}^{[n]}; \epsilon)\) converges monotonically to \(g_p(\hat{v}^*; \epsilon)\) for some KKT point \(\hat{v}^*\).

**Proof:** Please refer to Appendix A for details.

IV. GROUP SPARSE BEAMFORMING VIA LARGE SYSTEM ANALYSIS

In this section, we present the large system analysis for the iterative reweighted-\(\ell_2\) algorithm in Algorithm 1, thereby enabling RRH ordering only based on statistical CSI. In this way, the ordering criterion will change only when the long-term channel attenuation is updated, and thus it can further reduce the computational complexity of group sparse beamforming. The main novelty of this section is providing the closed-forms for the asymptotic analysis of the optimal Lagrangian multipliers based on the recent results in [27], thereby providing explicit expressions for the asymptotic RRH ordering results.

A. Deterministic Equivalent of Optimal Parameters

In this subsection, we provide asymptotic analysis for the optimal beamforming parameters \(p_k\)'s (19) and \(\lambda_k\)'s (21) when \(N \to \infty\). In a Cloud-RAN with distributed RRHs, the channel can be modeled as \(h_k = \Theta_k^{\frac{1}{2}} g_k, \forall k\), where \(g_k \sim \mathcal{CN}(0, I_{NL})\) is the small-scale fading and \(\Theta_k = \text{diag}(d_{k1}, \ldots, d_{kL}) \otimes I_N\) with \(d_{kl}\) as the path-loss from RRH \(l\) to MU \(k\). With this channel model, we have the following result for the deterministic equivalent of the \(\lambda\)-parameter.

**Lemma 1** (Asymptotic Results for \(\lambda\)-Parameter): Assume
\[
0 \leq \lim \inf_{N \to \infty} K/N \leq \lim \sup_{N \to \infty} K/N < \infty.
\]
Let \(\{d_{kl}\}\) and \(\{\gamma_k\}\) satisfy \(\lim \sup_{N \to \infty} \max_{1 \leq l \leq K} d_{kl} < \infty\) and \(\lim \sup_{N \to \infty} \max_{1 \leq k \leq K} \gamma_k < \infty\), respectively. We have \(\max_{1 \leq l \leq K} |\lambda_k - \lambda_k^0| \to 0\) almost surely, where \(\lambda_k^0\) is given by
\[
\lambda_k^0 = \left(\frac{1}{L} \sum_{l=1}^{L} d_{kl} \gamma_l\right)^{-1}. \tag{23}
\]
Here, $\eta_{l}$ is the unique solution of the following set of equations:
\[
\eta_l = \left( \frac{1}{NL} \sum_{i=1}^{K} \frac{d_{il}}{L} \gamma_i + \omega_l^{[n]} \right)^{-1}. \tag{24}
\]

**Proof:** Please refer to Appendix B for details.

Based on the above results, we further have the following asymptotic result for the optimal powers $p_k$’s.

**Lemma 2 (Asymptotic Results for Optimal Powers):** Let $\Delta \in \mathbb{C}^{K \times K}$ be such that
\[
[\Delta]_{k,l} := \frac{1}{NL} \frac{\gamma_i}{(1 + \gamma_k)^2} \psi_{ik}'.
\tag{25}
\]
If and only if $\limsup_K \|\Delta\|_2 < 1$, then $\max_k |p_k - p_k^{\ast} N \rightarrow 0$ almost surely, where $p_k$ is given by
\[
p_k = \gamma_k \psi_k' \left( \frac{1}{1 + \gamma_k^2} + \alpha_k^2 \right).
\tag{26}
\]
Here $\psi_k$, $\psi_k'$ and $\psi_{ik}'$ are given as follows:
\[
\psi_k = \frac{1}{L} \sum_{l=1}^{L} d_{kl} \eta_l,
\tag{27}
\]
and
\[
\psi_k' = \frac{1}{L} \sum_{l=1}^{L} d_{kl} \eta_l^2 + \frac{1}{NL} \sum_{j=1}^{K} \frac{2 \psi_{jk}''}{(1 + \gamma_j)^2 L} \sum_{l=1}^{L} d_{jl} \eta_l^2,
\tag{28}
\]
and
\[
\psi_{ik}' = \frac{1}{L} \sum_{l=1}^{L} d_{kl} \eta_l^2 + \frac{1}{NL} \sum_{j=1}^{K} \frac{2 \psi_{jk}''}{(1 + \gamma_j)^2} \sum_{l=1}^{L} d_{jl} \eta_l^2,
\tag{29}
\]
respectively; and $\tau = [\tau_1, \ldots, \tau_K]^T$ is given as
\[
\tau = \sigma^2 (I_K - \Delta)^{-1} \delta,
\tag{30}
\]
where $\delta = [\delta_1, \ldots, \delta_K]^T$ with
\[
\delta_k = \frac{1}{NL} \sum_{i=1}^{K} \gamma_i \psi_{ik}' \psi_{ik}^{-1}.
\tag{31}
\]

**Proof:** Please refer to Appendix C for details.

**B. Statistical CSI Based Group Sparse Beamforming Algorithm**

Based on the deterministic equivalents of the optimal beamforming parameters $\lambda_k$’s and $p_k$’s in Lemma 1 and Lemma 2, respectively, we have the following theorem on the squared $\ell_2$-norm of the solution to problem $\mathcal{P}^{[n]}_{\text{GSBF}}$, i.e.,
\[
\|\tilde{\psi}_{1}^{[n]}\|_2^2, \ldots, \|\tilde{\psi}_{L}^{[n]}\|_2^2.
\]

**Theorem 2 (Asymptotic Results for the Beamformers):** At the $n$-th iteration, for the squared $\ell_2$-norm of the solution to problem $\mathcal{P}^{[n]}_{\text{GSBF}}$, $\|\tilde{\psi}_{1}^{[n]}\|_2^2, \ldots, \|\tilde{\psi}_{L}^{[n]}\|_2^2$, we have
\[
\max_l \left\| \tilde{\psi}_{l}^{[n]} \right\|_2^2 \overset{N \rightarrow \infty}{\longrightarrow} 0 \text{ almost surely}
\]
\[
\tilde{\psi}_{l}^{[n]} = \frac{1}{NL} \sum_{k=1}^{K} p_k \psi_{lk} \psi_{lk}'
\tag{32}
\]
where $\psi_{lk} = \frac{1}{NL} d_{kl} \eta_l^2 + \frac{1}{NL} \sum_{j=1}^{K} \frac{\tilde{\psi}_{jk}''}{(1 + \gamma_j)^2} \sum_{l=1}^{L} d_{jl} \eta_l^2$.

**Proof:** Please refer to Appendix D for details.

We thus have the following deterministic equivalent of the weights $\omega_l^{[n]}$’s (11):
\[
\tilde{\omega}_{l}^{[n]} = \frac{p \psi_{l}^{[n]} \left( \tilde{\psi}_{l}^{[n]} + \epsilon^2 \right)}{2}, \quad \forall l = 1, \ldots, L.
\tag{33}
\]
Note that the asymptotic results of the powers $p_k$’s (26) and Lagrangian multipliers $\lambda_k$’s (23) should depend on the weights $\bar{\omega}_l^{[n]}$’s (33) at each iteration. Based on (7), we have the following asymptotic result for the RRH ordering criterion:
\[
\bar{\theta}_l = \kappa \tilde{\psi}_{l}^{[n]},
\tag{34}
\]
where $\tilde{\psi}_{l}^{[n]}$ is the deterministic equivalent of the squared $\ell_2$-norm of the solution to problem $\mathcal{P}^{[n]}_{\text{GSBF}}$ using the iterative reweighted-$\ell_2$ algorithm. Therefore, the RRH with a smaller $\bar{\theta}_l$ will have a higher priority to be switched off. This ordering criterion will change only when the long-term channel attenuation is updated. Note that global instantaneous CSI is still needed in stage II to find the active RRHs, i.e., solving a sequence of convex feasibility problems $\mathcal{F}_l(A^{[n]})$ (8).

The statistical CSI based iterative reweighted-$\ell_2$ algorithm for group sparse beamforming is presented in Algorithm 2.

**Algorithm 2 Statistical CSI Based Iterative Reweighted-$\ell_2$ Algorithm for Problem $\mathcal{P}^{[n]}_{\text{GSBF}}$**

**input:** Initialize $\omega^{[0]} = (1, \ldots, 1)$; $I$ (the maximum number of iterations)

Repeat
1) Compute deterministic equivalent of the squared $\ell_2$-norm of the solution to $\mathcal{P}^{[n]}_{\text{GSBF}}$, $\|\tilde{\psi}_{1}^{[n]}\|_2^2, \ldots, \|\tilde{\psi}_{L}^{[n]}\|_2^2$ using $\tilde{\omega}_l^{[n]}$ (32).
2) Update the weights $\bar{\omega}_l^{[n+1]}$ using (33).

Until convergence or attain the maximum iterations and return

**output:** Asymptotic result of the RRH ordering criterion $\bar{\theta}$ (34).

**Remark 3:** Although stage 2 and stage 3 still require instantaneous CSI, the RRH ordering criterion computed by Algorithm 2 in stage 1 is only based on statistical CSI and thus will be updated only when the long-term channel propagation is changed. Therefore, Algorithm 2 serves the purpose of further reducing the computation complexity of Algorithm 1 for RRH ordering. A promising future research direction is to select RRHs in stage 2 only based on statistical CSI. However, the main challenge is the infeasibility issue if only statistical CSI is available, as discussed in Remark 1.

**V. SIMULATION RESULTS**

In this section, we will simulate the proposed algorithms for network power minimization for Cloud-RANs. In all the realizations, we only account the channel realizations making the original problem $\mathcal{P}$ feasible. If problem $\mathcal{P}$ is infeasible, further works on user admission are required [15]. We set...
The proposed iterative reweighted-$\ell_2$ algorithms (Algorithm 1 and Algorithm 2) will terminate if either the number of iterations exceeds 30 or the difference between the objective values of consecutive iterations is less than $10^{-3}$.

A. Convergence of the Iteratively Reweighted-$\ell_2$ Algorithm

Consider a network with $L = 5$ 30-antenna RRHs and 5 single antenna MUs uniformly and independently distributed in the square region $[-2000, 2000] \times [-2000, 2000]$ meters. Fig. 2 shows the convergence of the iterative reweighted-$\ell_2$ algorithm in different scenarios with different realizations of RRH and MU positions. For each scenario, the numerical results are obtained by averaging over 100 small-scale fading realizations. The large-scale fading (i.e., statistical CSI) is randomly generated and fixed during simulations. In the two curves of each scenario, Algorithm 1 and Algorithm 2 are applied for Stage I of group sparse beamforming, respectively. It demonstrates that the large system analysis based Algorithm 2 provides accurate approximation even in a small system. Fast convergence is observed in the simulated setting.

B. Network Power Minimization

Consider a network with $L = 5$ 10-antenna RRHs and 6 single antenna MUs uniformly and independently distributed in the square region $[-1000, 1000] \times [-1000, 1000]$ meters. The relative transport link power consumption are set to be $P^l_l = (5.6 + 2/l)W$, $l = 1, \ldots, L$. We average over 200 small-scale channel realizations. Fig. 3 demonstrates the average network power consumption using different algorithms. This figure shows that the proposed iterative reweighted-$\ell_2$ algorithm outperforms the weighted mixed $\ell_1/\ell_2$-norm algorithm in [7]. Furthermore, it illustrates that the large system analysis provides accurate approximations. Although the simulated results demonstrate that the performance is robust to different values of parameter $p$, it is very interesting to theoretically identify the typical scenarios, where smaller values of parameter $p$ will yield much lower network power consumption.

VI. Conclusions and Discussions

In this paper, we developed an enhanced three-stage group sparse beamforming framework with reduced computation overhead in Cloud-RANs. In particular, closed-form solutions for the group sparse optimization problem were obtained by developing the iterative reweighted-$\ell_2$ algorithm based on the MM algorithm and Lagrangian duality theory. This is the first effort to reduce the computation cost for RRH ordering in the first stage of group sparse beamforming. Based on the developed structured iterative algorithm, we further provided a large system analysis for the optimal Lagrangian multipliers at each iteration via random matrix theory, thereby computing the RRH ordering criterion only based on the statistical CSI. This is the second effort to enable computation scalability for RRH ordering in the first stage.

Several future directions of interest are listed as follows:

- Although computing the RRH ordering criterion in the first stage with Algorithm 2 only needs statistical CSI, the second stage still requires global instantaneous CSI
to find the active RRHs by solving a sequence of convex feasibility problems. It is thus particularly interesting to investigate efficient algorithms to select the active RRHs only based on the statistical CSI.

- It is desirable to establish the optimality of the iterative reweighted-ℓ₂ algorithm for the network power minimization problem \( \mathcal{P} \). However, considering the complicated problem structures of problem \( \mathcal{P} \), this becomes challenging. It is also interesting to apply the developed statistical CSI based iterative reweighted-ℓ₂ algorithm for more complicated network optimization problems, e.g., the wireless caching problem [33], [34], the computation offloading problem [36], and beamforming problems with CSI uncertainty [32].

\section*{Appendix A}

\subsection*{Proof of Theorem 1}

1) Observing that the phases of \( \mathbf{v}_k \) will not change the objective function and constraints of problem \( \mathcal{P}_{\text{GSBF}} \), the QoS constraints thus can be equivalently transformed to the second-order cone constraints:

\[ C = \left\{ \mathbf{v} : \sum_{k \neq k'} |h_k^\dagger \mathbf{v}_k|^2 + \sigma_k^2 \leq \mathcal{R}(h_k^\dagger \mathbf{v}_k)/\gamma_k, \forall k \right\}, \]

which are second-order cones. The KKT points of problem \( \mathcal{P}_{\text{GSBF}} \) should satisfy:

\[ 0 \in \nabla_v g_p(\mathbf{v}; \epsilon) + \mathcal{N}_C(\mathbf{v}), \]

where \( \mathcal{N}_C(\mathbf{v}) \) is the normal cone of the second-order cone at point \( \mathbf{v} \) [47]. We shall show that any convergent subsequence \( \{\mathbf{v}^{[n]}\}_{n=1}^{[\infty]} \) of \( \{\mathbf{v}^{[n]}\}_{n=1}^{[\infty]} \) satisfies (35). Specifically, let \( \mathbf{v}^{[n]} \rightarrow \bar{\mathbf{v}} \) be one such convergent subsequence with

\[ \lim_{k \rightarrow \infty} |v^{[n]}| = \lim_{k \rightarrow \infty} |v^{[n]}| = \bar{v}. \]

Based on the strong duality result for problem \( \mathcal{P}_{[n]} \), the following KKT condition holds at \( \mathbf{v}^{[n+1]} \):

\[ 0 \in \nabla_v Q(\mathbf{v}^{[n+1]}, \omega^{[n]}) + \mathcal{N}_C(\mathbf{v}^{[n+1]}). \]

Based on (36) and (11), we have

\[ \lim_{k \rightarrow \infty} \nabla_v Q(\mathbf{v}^{[n+1]}, \omega^{[n]}) = \nabla_v g_p(\bar{\mathbf{v}}, \epsilon). \]

Furthermore, based on [47, Proposition 6.6] and (36), we have

\[ \lim_{n \rightarrow \infty} |v^{[n]}| = \lim_{n \rightarrow \infty} |v^{[n]}| = \mathcal{N}_C(\bar{v}). \]

Therefore, by taking \( k \rightarrow \infty \) in (37), we have \( 0 \in \nabla_v Q(\bar{\mathbf{v}}, \bar{\omega}) + \mathcal{N}_C(\bar{v}) \), which indicates that \( \bar{v} \) is a KKT point of problem \( \mathcal{P}_{\text{GSBF}} \). We thus complete the proof.

2) We first conclude the following fact:

\[ g_p(\mathbf{v}^{[n+1]}, \epsilon) = \mathcal{Q}(\mathbf{v}^{[n+1]}, \omega^{[n]}) + g_p(\mathbf{v}^{[n+1]}, \epsilon) - \mathcal{Q}(\mathbf{v}^{[n+1]}, \omega^{[n]}) \leq \mathcal{Q}(\mathbf{v}^{[n+1]}, \omega^{[n]}) + g_p(\mathbf{v}^{[n+1]}, \epsilon) - \mathcal{Q}(\mathbf{v}^{[n+1]}, \omega^{[n]}) \leq \mathcal{Q}(\mathbf{v}^{[n+1]}, \omega^{[n]}) + g_p(\mathbf{v}^{[n+1]}, \epsilon) - \mathcal{Q}(\mathbf{v}^{[n+1]}, \omega^{[n]}) = g_p(\mathbf{v}^{[n+1]}, \epsilon), \]

where the first inequality is based on the fact that function \( g_p(\mathbf{v}^{[n+1]}, \epsilon) - \mathcal{Q}(\mathbf{v}^{[n+1]}, \omega^{[n]}) \) attains its maximum at \( \mathbf{v} = \mathbf{v}^{[n]} \) [15, Proposition 1], and the second inequality follows from (37). Furthermore, as \( g_p(\mathbf{v}; \epsilon) \) is continuous and \( C \) is compact, the limit of the sequence \( g_p(\mathbf{v}^{[n+1]}, \epsilon) \) is finite. Based on the convergence results in 1), we thus complete the proof.

\section*{Appendix B}

\subsection*{Proof of Lemma 1}

The proof technique here is mainly based on the work [26]. However, we have to modify their proof as we have different weighting matrices \( \mathbf{Q}^{[n]} \) in vectors \( \bar{v}_k \) (16) at the \( n \)-th iteration and such modification is non-trivial. Based on the following matrix inversion lemma [48], \( \mathbf{x}^H(U + \epsilon xx^H)^{-1} = \mathbf{x}^H(U^{-1} - \frac{1}{1 + xx^H}) \).

(21) can be rewritten as

\[ \gamma_k \frac{\lambda_k^2}{\lambda_k^2} = \frac{1}{LN} h_k^H \left( \frac{1}{LN} \sum_{i \neq k} \lambda_i h_i h_i^H + Q \right)^{-1} h_k, \]

which can be further rewritten as

\[ \gamma_k \rho_k = \frac{\lambda_k^2}{\lambda_k^2} \left( \frac{1}{LN} \sum_{i \neq k} \rho_i h_i h_i^H + Q \right)^{-1} h_k. \]

Assume that \( 0 \leq \rho_1 \leq \rho_2 \leq \cdots \leq \rho_K \). From (40), replacing \( \rho_i \) with \( \rho_K \) and using monotonicity arguments, we have

\[ \gamma_k \rho_K \leq \frac{\lambda_k^2}{\lambda_k^2} \left( \frac{1}{LN} \sum_{i \neq k} \rho_i h_i h_i^H + Q \right)^{-1} h_k. \]

or, equivalently

\[ \gamma_k \leq \frac{\lambda_k^2}{\lambda_k^2} \left( \frac{1}{LN} \sum_{i \neq k} \rho_i h_i h_i^H + \rho_K Q \right)^{-1} h_k. \]

Assume now that \( \rho_K \) is infinitely often larger than \( (1 + \ell) \) with \( \ell \) being some positive value [27]. Let us restrict ourselves to such a subsequence. From (42), using monotonicity arguments we obtain

\[ \gamma_k \leq \frac{\lambda_k^2}{\lambda_k^2} \left( \frac{1}{LN} \sum_{i \neq k} \rho_i h_i h_i^H + (1 + \ell) Q \right)^{-1} h_k. \]

Define

\[ m_k(\ell) = \frac{1}{LN} h_k^H \left( \frac{1}{LN} \sum_{i \neq k} \rho_i h_i h_i^H + (1 + \ell) Q \right)^{-1} h_k. \]

Now we investigate the deterministic equivalents for \( m_k(\ell) \). We first introduce the following important lemma:

\[ \text{Lemma 3 (23, Lemma 14.2)): Let } A_1, A_2, \ldots, \text{ with } A_\infty \in \mathbb{C}^{N \times N} \text{ be a series of random matrices generated by the probability space } (\Omega, \mathcal{F}, P) \text{ such that, for } \omega \in A \subset \Omega, \text{ with } P(A) = 1, \|A_N(\omega)\| < K(\omega) < \infty, \text{ uniformly on } N. \text{ Let } x_1, x_2, \ldots, \text{ with } x_\in \mathbb{C}^N, \text{ be random vectors of i.i.d. entries with zero mean, variance } 1/N, \text{ and the eighth-order moment of order } O(1/N^4), \text{ independent of } A_N. \text{ Then}

\[ x_N^H A_N x_N - \frac{1}{N} \text{Tr}(A_N) \xrightarrow{N \to \infty} 0, \]

almost surely.
Therefore, based on Lemma 3, we have
\[
m_K(\ell) - \frac{1}{LN} \text{Tr} \Theta_K \left( \frac{1}{LN} \sum_{i \neq K} J^*_i b_i h_i^H + (1 + \ell)Q \right)^{-1} \xrightarrow{N \to \infty} 0.
\]  

(46)

We further introduce the following important lemma to derive the deterministic equivalent for the \( m_K(\ell) \).

**Lemma 4 (24, Th. 1):** Let \( X_N = X_N^H X_N + S_N \) with \( S_N \in C^{N \times N} \) Hermitian nonnegative definite and \( X_N \in C^{n \times N} \) random. The \( i \)-th column of \( X_N \) is \( x_i = \Psi_i y_i \), where the entries of \( y_i \in C^n \) are i.i.d. of zero mean, variance \( 1/N \) and have eighth-order moment of order \( O(1/N^4) \). The matrices \( \Psi_j \in C^{N \times r_i} \) are deterministic. Furthermore, let \( \Theta_i = \Psi_i \Psi_i^H \in C^{N \times N} \) and define \( Q_N \in C^{N \times N} \) deterministic. Assume \( \lim \sup_{N \to \infty} \sup_{1 \leq i < n} \|\Theta_i\| < \infty \) and let \( Q_N \) have uniformly bounded spectral norm (with respect to \( N \)). Define
\[
m_{B_N, Q_N}(z) := \frac{1}{N} \text{Tr} Q_N (B_N - z I_N)^{-1}.
\]  

(47)

Then, for \( z \in \mathbb{C} \setminus \mathbb{R}^+ \), as \( n, N \) grow large with ratios \( \beta_{N,i} := N/r_i \) and \( \beta_N := N/n \) such that \( 0 < \lim \inf_{N \to \infty} \beta_N \leq \lim \sup_{N \to \infty} \beta_N < \infty \) and \( 0 < \lim \inf_{N \to \infty} \beta_{N,i} \leq \lim \sup_{N \to \infty} \beta_{N,i} < \infty \), we have that
\[
m_{B_N, Q_N}(z) - m_{B_N, Q_N}(z) \xrightarrow{N \to \infty} 0
\]  

(48)

almost surely, with \( m_{B_N, Q_N}(z) \) given by
\[
m_{B_N, Q_N}(z) = \frac{1}{N} \text{Tr} Q \left( \frac{1}{N} \sum_{j = 1}^{n} \frac{\Theta_j}{1 + e_{N,j}(z)} + S_N - z I_N \right)^{-1},
\]  

(49)

where the functions \( e_{N,1}(z), \ldots, e_{N,n}(z) \) from the unique solution of
\[
e_{N,i}(z) = \frac{1}{N} \text{Tr} \Theta_i \left( \frac{1}{N} \sum_{j = 1}^{n} \frac{\Theta_j}{1 + e_{N,j}(z)} + S_N - z I_N \right)^{-1},
\]  

(50)

which is the Stieltjes transform of a nonnegative finite measure on \( \mathbb{R}^+ \). Moreover, for \( z < 0 \), the scalars \( e_{N,1}(z), \ldots, e_{N,n}(z) \) are unique nonnegative solutions to (50).

Therefore, based on Lemma 4, we have
\[
\psi_K(\ell) - \psi^o_K(\ell) \xrightarrow{N \to \infty} 0
\]  

(51)

almost surely with \( \psi^o_K(\ell) \) being the unique positive solution to
\[
\psi^o_K(\ell) = \frac{1}{NL} \text{Tr}(\Theta_K A(\ell)),
\]  

(52)

where
\[
A(\ell) = \left( \frac{1}{NL} \sum_{i \neq K} J^*_i \Theta_i}{1 + J^*_i \psi^o_K(\ell)} + (1 + \ell)Q \right)^{-1}.
\]  

(53)

From (51), recalling (43) yields
\[
\lim_{K \to \infty} \inf_{\ell} \psi^o_K(\ell) \geq \gamma_K/\lambda^o_K.
\]  

(54)

Using the fact that \( \psi^o_K(\ell) \) is a decreasing function of \( \ell \), it can be proved [23] that for any \( \ell > 0 \), we have
\[
\lim_{K \to \infty} \sup_{\ell} \psi^o_K(\ell) < \gamma_K/\lambda^o_K.
\]  

(55)

However, this is against the former condition and creates a contradiction on the initial hypothesis that \( \rho_K < 1 + \ell \) infinitely often. Therefore, we must admit that \( \rho_K \leq 1 + \ell \) for all large values of \( K \). Reverting all inequalities and using similar arguments yields \( \rho_K \geq 1 - \ell \) for all large values of \( K \).

We eventually obtain that \( 1 - \ell \leq \rho_K \leq 1 + \ell \) from which we may write \( \max |\rho_K - 1| \leq \ell \) for all large values of \( K \). Taking a countable sequence of \( \ell \) going to zero yields \( \max |\rho_K - 1| \to 0 \) from which using \( \rho_K = \lambda^o_K/\lambda_K \) and assuming \( \lim_{K \to \infty} \sup_{\ell} \gamma_K < \infty \), we obtain
\[
\max |\lambda_K - \lambda^o_K| \xrightarrow{N \to \infty} 0,
\]  

(56)

almost surely. From (40), we have \( \gamma_K/\lambda^o_K = \psi^o_K(0) \psi^o_K \). Therefore, we obtain \( \lambda^o_K = \gamma_K/\psi^o_K \), where \( \psi^o_K \) is the solution of the following equation:
\[
\psi^o_K = \frac{1}{NL} \text{Tr}(\Theta_K A) = \frac{1}{L} \sum_{l = 1}^{L} d_{kl} \eta_l.
\]  

(57)

Following the same steps for \( k = 1, \ldots, K \) yields the following desired result:
\[
\lambda^o_K = \gamma_k/\psi^o_K, \quad \forall k.
\]  

(58)

As \( \Theta_k = \text{diag}(d_{1k}, \ldots, d_{Lk}) \otimes I_N \), we have
\[
\psi^o_K = \frac{1}{NL} \text{Tr}(\Theta_k A) = \frac{1}{L} \sum_{l = 1}^{L} d_{kl} \eta_l.
\]  

(59)

where \( A = A(0) \) in (53) and \( \{\eta_l\} \) is the unique positive solution to the following set of equations
\[
\eta_l = \left( \frac{1}{NL} \sum_{i = 1}^{K} d_{il} \frac{\gamma_i}{1 + \gamma_i} + \sigma^2 \right)^{-1}.
\]  

(60)

We thus complete the proof for the asymptotic results of the optimal Lagrange multipliers in Lemma 1.

**APPENDIX C**

**Proof of Lemma 2**

The SINR for MU \( k \) (2) can be rewritten as
\[
\sinr_k = \frac{p_k}{\sum_{i \neq k} \frac{p_i |h_i^H v_i|^2}{||v_i||_2^2} + \sigma^2}.
\]  

(61)

where \( \tilde{v}_k = \left( \sum_{i = 1}^{K} \frac{\lambda^o_i}{\gamma_i} h_i h_i^H + Q^{1/2} \right)^{-1} h_k \). The interference part of the denominator of \( \sinr_k \) in (61) can be rewritten as
\[
\frac{1}{NL} \sum_{i \neq k} \frac{p_i |h_i^H v_i|^2}{||v_i||_2^2} = \frac{1}{NL} \sum_{i \neq k} p_i h_k^H \left( \tilde{v}_k \tilde{v}_k^H \right) h_k
\]  

(62)
with \( V = \left( \frac{1}{NL} \sum_{i=1}^{K} x_i h_i^H + Q \right)^{-1} \), \( \Theta[1] := \frac{1}{NL} \text{Tr} \left( \Theta_1 V[k] \right) \) and \( \mu' = \frac{1}{NL} \text{Tr} \left( \frac{1}{NL} \text{Tr} \left( \Theta_1 \left( V[k] - 2 \mu^* \frac{1}{NL} \text{Tr} \left( \Theta_1 V[k] \right) \right) \right) \right) \). Furthermore, we have

\[
\frac{1}{NL} h_k^H (V[k] - 2 \mu^* \frac{1}{NL} \text{Tr} \left( \Theta_1 V[k] \right) \right) h_k \rightarrow 0 \quad \text{almost surely.}
\]

Based on the results in (65), (68), (69), we have

\[
\frac{1}{NL} h_k^H (V[k] - 2 \mu^* \frac{1}{NL} \text{Tr} \left( \Theta_1 V[k] \right) \right) h_k \rightarrow 0 \quad \text{almost surely.}
\]

From Lemma 1, we have \( \mu - \psi_k^N \frac{N}{\sqrt{L}} \rightarrow 0 \) almost surely. Applying [24, Lemma 6], we have

\[
\frac{1}{NL} \text{Tr} \left( \frac{1}{NL} \text{Tr} \left( \Theta_1 \left( V[k] - 2 \mu^* \frac{1}{NL} \text{Tr} \left( \Theta_1 V[k] \right) \right) \right) \right) \rightarrow 0 \quad \text{almost surely.}
\]

Further, we have

\[
\frac{1}{NL} h_k^H \left( V[k] - 2 \mu^* \frac{1}{NL} \text{Tr} \left( \Theta_1 V[k] \right) \right) h_k \rightarrow 0 \quad \text{almost surely.}
\]

Applying [24, Lemma 1 and 4], we obtain almost surely

\[
\frac{1}{NL} h_k^H \left( V[k] - 2 \mu^* \frac{1}{NL} \text{Tr} \left( \Theta_1 V[k] \right) \right) h_k \rightarrow 0 \quad \text{almost surely.}
\]

To derive a deterministic equivalent for \( \frac{1}{NL} \text{Tr} \left( \Theta_1 (V[k] - 2 \mu^* \frac{1}{NL} \text{Tr} \left( \Theta_1 V[k] \right) \right) \right) \), we write

\[
\frac{1}{NL} \text{Tr} \left( \Theta_1 (V[k] - 2 \mu^* \frac{1}{NL} \text{Tr} \left( \Theta_1 V[k] \right) \right) \right) \rightarrow 0 \quad \text{almost surely.}
\]

Observe now that [24, Theorem 1]

\[
\text{Tr} \left( \Theta_1 (V[k] - 2 \mu^* \frac{1}{NL} \text{Tr} \left( \Theta_1 V[k] \right) \right) \rightarrow 0 \quad \text{almost surely.}
\]

where \( \psi_{ik}(z) \) is given by

\[
\frac{1}{NL} \text{Tr} \left( \Theta_1 (V[k] - 2 \mu^* \frac{1}{NL} \text{Tr} \left( \Theta_1 V[k] \right) \right) \right) \rightarrow 0 \quad \text{almost surely.}
\]

Therefore, applying Lemma 5, we obtain that

\[
\frac{1}{NL} h_k^H (V[k] - 2 \mu^* \frac{1}{NL} \text{Tr} \left( \Theta_1 V[k] \right) \right) h_k \rightarrow 0 \quad \text{almost surely.}
\]
where
\[ T_k'(0) = T_k(0) \left( \frac{1}{|N| L} \sum_{j=1}^{K} \frac{\lambda_j^2 \psi_j^2(0) \Theta_j}{(1 + \gamma_j)^2} + \Theta_k \right) T_k(0). \]

In writing the above result, we have taken into account that
\[ A = T_j(0), \psi_j(0) = \frac{1}{|N| L} \text{Tr}(\Theta_j T_k(0)) = \frac{1}{|N| L} \text{Tr}(\Theta_j A), \quad \psi_j^2 = \lambda_j^2 \psi_j, \]
and \( \gamma_j = \lambda_j^2 \psi_j^2 \). Plugging (79) into (78) and neglecting the functional dependence from \( z = 0 \), \( \Psi_k = [\psi_{ik}\ldots, \psi_{kk}^T] \) is found as the unique solution of
\[
\psi_{ik}' = \frac{1}{|N| L} \text{Tr} \left( \Theta_j A \left( \frac{1}{|N| L} \sum_{j=1}^{K} \frac{\lambda_j^2 \psi_j^2(0) \Theta_j}{(1 + \gamma_j)^2} + \Theta_k \right) A \right)
= \frac{1}{|N| L} \text{Tr}(\Theta_j A \Theta_j A)
+ \frac{1}{|N| L} \sum_{j=1}^{K} \frac{\lambda_j^2 \psi_j^2}{(1 + \gamma_j)^2} \frac{1}{|N| L} \text{Tr} \left( \Theta_i A \Theta_j A \right).
\]

Observing that
\[ \frac{1}{|N| L} \text{Tr}(\Theta_j A \Theta_j A) = \frac{1}{L} \sum_{i=1}^{L} d_{ij} d_{ji} \eta_i^2. \]

Let \( \Psi_k = [\psi_{ik}', \ldots, \psi_{kk}']^T \in \mathbb{C}^K \) and \( J = [J_{ij}] \in \mathbb{C}^{K \times K} \)

with
\[ J_{ij} = \frac{\lambda_i^2}{|N| L(1 + \gamma_i)^2} \left( \frac{1}{L} \sum_{i=1}^{L} d_{ij} d_{ji} \eta_i^2 \right). \]

We can rewrite the above system of equations in the compact form as
\[ \Psi_k = C_k + J \Psi_k', \]
where \( C_k = [c_{ik}] \) with \( c_{ik} = \frac{1}{L} \sum_{i=1}^{L} d_{ij} d_{ji} \eta_i^2 \).

On the basis of above results, using \( \frac{1}{|N| L} \text{Tr}(\Theta_j A) - \gamma_j \to 0 \), we eventually obtain that
\[ \frac{1}{|N| L} h_k^H V \Theta_j V h_k - \frac{\psi_{jk}'}{(1 + \gamma_j)^2} \xrightarrow{N \to \infty} 0 \]
almost surely. Following similar arguments of above yields
\[ \frac{1}{|N| L} h_k^H V^2 h_k - \frac{\psi_{kk}'}{(1 + \gamma_k)^2} \xrightarrow{N \to \infty} 0 \]
almost surely with \( \psi' = [\psi_1', \ldots, \psi_K']^T = (I_K - J)^{-1} e \) where \( e \in \mathbb{C}^K \) has elements \( e_i = \frac{1}{L} \sum_{i=1}^{L} d_{ii} \eta_i^2 \).

Putting the results in (84) and (85) together, we obtain almost surely
\[ \frac{1}{|N| L} \sum_{i \neq k} p_i \frac{1}{|N| L} h_k^H \Theta_j V h_k - \frac{1}{|N| L} \sum_{i \neq k} p_i \frac{\psi_j'}{\psi_i} \xrightarrow{N \to \infty} 0. \]

The deterministic equivalent of the numerator of the SINR in (61) is now easily obtained as
\[ p_k \frac{1}{|N| L} h_k^H V h_k \xrightarrow{N \to \infty} 0 \quad \text{and} \quad \frac{\psi_{kk}^2}{(1 + \gamma_k)^2} \xrightarrow{N \to \infty} 0 \]
almost surely.

Therefore, the deterministic equivalent SINR is given by
\[ \sin r_k^2 = \frac{\psi_{kk}^2}{p_k} \frac{p_k}{I_k^2 + \sigma_k^2}, \]

where
\[ I_k^2 := \frac{1}{(1 + \gamma_k)^2} \left( \frac{1}{|N| L} \sum_{i=1}^{K} \frac{p_i \psi_i'}{\psi_i} \right). \]

From (88), it follows that \( p_k^2 \) such that \( \sin r_k^2 = \gamma_k \) is obtained as
\[ p_k^2 = \frac{\psi_{kk}}{\psi_{kk}^2} (I_k^2 + \sigma_k^2), \]
which can be further rewritten as
\[ p_k^2 \frac{\psi_{kk}^2}{\gamma_k} = I_k^2 + \sigma_k^2 = \frac{1}{(1 + \gamma_k)^2} \left( \frac{1}{|N| L} \sum_{i=1}^{K} p_i \psi_i' \right) + \sigma_k^2. \]

Therefore, the deterministic equivalent for the powers is given by
\[ \begin{bmatrix} p_k^2 \\ \vdots \\ p_k^2 \end{bmatrix} = M^{-1} \begin{bmatrix} \sigma_k^2 \\ \vdots \\ \sigma_k^2 \end{bmatrix}, \]
where
\[ [M^c]_{ij} = \begin{cases} \frac{1}{1 + (\gamma_i^2) L N} \psi_i', & i = j, \\ \frac{1}{(1 + \gamma_i^2) L N} \psi_j', & i \neq j. \end{cases} \]

We thus complete the proof for the asymptotic results for optimal powers in Lemma 2.

**APPENDIX D**

**PROOF OF THEOREM 2**

We rewrite \( \|\tilde{v}_i\|^2 \) as
\[ \|\tilde{v}_i\|^2 = \frac{\sum_{k=1}^{K} q_{ik} V h_k}{|N| L} \left( \frac{1}{|N| L} \sum_{k=1}^{K} \frac{p_k \tilde{v}_k^H Q_{ik} \tilde{v}_k}{\|\tilde{v}_k\|^2} \right) \]
\[ = \frac{1}{|N| L} \sum_{k=1}^{K} h_k^H Q_{ik} h_k. \]

where \( Q_{ik} \in \mathbb{C}^{NL \times NL} \) is a block diagonal matrix with the identify matrix \( I_N \) as the \( l \)-th main diagonal block square matrix and zeros elsewhere.

Based on the similar arguments in Appendix C, we have the deterministic equivalents
\[ h_k^H Q_{ik} h_k \xrightarrow{N \to \infty} 0, \]
where
\[ \psi_{kl} = \frac{1}{|N| L} \text{Tr}(\Theta_j A Q_{ik} A) \]
\[ = \frac{1}{|N| L} \sum_{j=1}^{K} \frac{\lambda_j^2 \psi_j}{(1 + \gamma_j)^2} \frac{1}{|N| L} \text{Tr}(\Theta_j A \Theta_j A). \]
Observing that
\[
\frac{1}{NL} \text{Tr}(\Theta_k A Q_k d_k \Lambda) = \frac{1}{L} \sum_{k=1}^L \|\eta_k\|^2,
\]
we obtain the final result. We thus complete the proof for the asymptotic results for \(\|v^*\|^2\) in Theorem 2.

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