Experimental investigation of spray characteristics of ethyl esters in a constant volume chamber

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Abstract
Biodiesels are mainly produced via the utilization of methanol in transesterification, which is the widespread biodiesel production process. The majority of this methanol is currently obtained from fossil resources, i.e. coal and natural gas. However, in contrast with methanol, biomass-based ethanol can also be used to produce biodiesels; this could allow the production line to become fully renewable. This study aimed to investigate the spray characteristics of various ethyl ester type biodiesels derived from sunflower and corn oils in comparison to methyl esters based on the same feedstocks and reference petroleum-based diesel. Spray penetration length (SPL) and spray cone angle (SCA) were experimentally evaluated in a constant volume chamber allowing optical access, under chamber pressures of 0, 5, 10 and 15 bar and injection pressures of 600 and 800 bar. Sauter mean diameter (SMD) values were estimated by using an analytical correlation. Consequently, ethyl esters performed longer SPL (2.8–20%) and narrower SCA (5.1–19%) than diesel under ambient pressures of 5 and 10 bar. Although the SMD values of ethyl esters were 48% higher than diesel on average, their macroscopic spray characteristics were very similar to those of diesel under 15 bar chamber pressure. Moreover, ethyl esters were found to be very similar to methyl esters in terms of spray characteristics. The differences in SPL, SCA and SMD values for both types of biodiesels were lower than 4%. When considering the uncertainty (± 0.84%) and repeatability (±5%) ratios, the difference between the spray characteristics of methyl and ethyl esters was not major.

Keywords Biodiesel · Ethyl ester · Methyl ester · Spray investigation · Constant volume chamber

1 Introduction

Conventional diesel fuel (petrodiesel) consumption has been one of the major sources of air pollution. As a result of petrodiesel combustion, various toxic gases, e.g. carbon monoxide (CO), hydrocarbons (HC), nitric oxides (NOx) and particulate matters (PM) are emitted to the atmosphere [1]. These pollutants contribute to serious environmental problems, as global warming is considered to be the most serious one for the planet. Hence, to mitigate such pollutant emissions, it is necessary to increase the share of alternative fuels that can directly be utilized in diesel engines. In this context, the major emerging alternative fuel for use in conventional diesel engines is biodiesel [2, 3]. Biodiesels are promising fuels addressing the aforementioned environmental concerns since they are renewable and biodegradable [4–6], reducing the harmful emissions [7–9] and having the ability to directly be utilized in existing diesel engines with little or no modifications [10, 11]. In 2019, total global biodiesel consumption was almost 104 thousand tonnes day⁻¹
methyl esters, such as having lower methyl and ethyl esters. Ethyl esters have some consideration in the transesterification process are respectively named biodiesels obtained via the utilization of methanol or ethyl alcohol. This ensures that the resulting biodiesel is fully renewable. Biodiesels obtained via the utilization of methanol or ethanol could be considered as an alternative for fossil-based methanol; also utilized [27]. For this reason, bio-based ethanol could be produced from maize (3%) and other grains, cassava or sugar beets, were the ethanol was produced from maize ([12]. Although ethanol production decreased globally almost by 15% in 2020 due to the COVID-19 outbreak [26], the production amount was still significant. In 2019, 123.36 billion litres of methanol were produced globally, and approximately 65% and 35% of methanol were respectively produced from natural gas and coal [24]. The amount of methanol produced from renewable energy sources was less than 1% [24]. In contrast, 109.89 billion litres of ethanol were produced in the world in 2019 [25]. Although ethanol production decreased globally almost by 15% in 2020 due to the COVID-19 outbreak [26], the production amount was still significant. In 2020, most of the ethanol was produced from maize (ca. 64%), and different feedstocks such as sugarcane (26%), molasses (3%), wheat (3%) and other grains, cassava or sugar beets, were also utilized [27]. For this reason, bio-based ethanol could be considered as an alternative for fossil-based methanol; this ensures that the resulting biodiesel is fully renewable. Biodiesels obtained via the utilization of methanol or ethanol in the transesterification process are respectively named methyl and ethyl esters. Ethyl esters have some considerable advantages over methyl esters, such as having lower iodine values, higher oxidation stabilities and better lubricity characteristics [21, 22]. As an important superiority, cloud, cold filter plugging and pour points of ethyl esters are also lower than those of methyl esters, making their cold flow properties better than that of the methyl esters [28, 29]. These advantages show that the use of bio-based ethanol in biodiesel production can be beneficial for their use in diesel engines. Despite their superiority and aforementioned advantages, published research studies concerning ethyl esters in terms of their use in diesel engines are limited compared to that of methyl esters. However, when considering performance and emission analysis according to existing research [30–38], ethyl esters could be considered as clear alternatives. Table 1 shows the existing literature studies, where the performance and emission characteristics of ethyl esters are compared with that of methyl esters. The table also compares some important physical and chemical properties like calorific values, viscosities and densities of both. For example, Sanli et al. [30] investigated the performance and emission characteristics of waste frying oil (WFO)-based ethyl ester and methyl ester biodiesels in a six-cylinder, four-stroke, water-cooled, turbocharged diesel engine. Differences between the physical and chemical properties of these fuels were minor. Ethyl ester had a 0.1% smaller density, 8.9% larger viscosity and 0.58% higher calorific value than methyl ester. When comparing the performance characteristics of these fuels, it was observed that ethyl ester performed a 2.38% reduction in brake specific fuel consumption and 1.98% advancement in brake thermal efficiency on average. For emission analysis, they found that ethyl ester emitted 8% less CO and 12.7% less HC on average than methyl ester, and NOx emissions were very close to each other for both fuels. The authors of the study explained that ethyl ester had slightly better results in terms of performance and emission characteristics than methyl ester originated from the same feedstock (i.e. WFO). Besides, Gautam et al. [32] investigated the performance and emission characteristics of methyl and ethyl ester type biodiesels originated from jatropha oil and their blends with petrodiesel in the ratios of 5, 10, 20 and 30 vol.% in a diesel engine. Pure ethyl ester had a 1% lower density, 5.3% higher viscosity and 0.8% higher calorific value compared to that of pure methyl ester. In this study, the optimum blend ratio was found as 20% for diesel/methyl ester and diesel/ethyl ester blends. BSFC values of B20 (i.e. blend containing 20 vol.% biodiesel) of methyl ester and ethyl ester were respectively 9.8% and 8.6% lower than that of petrodiesel. BTE values of B20 of methyl ester and ethyl ester were 11% and 9.3% higher than that of diesel fuel, respectively. Consequently, the performance characteristics of ethyl and methyl esters were found to be close to each other. Besides, NOx, CO, HC and PM emissions were very similar for both ethyl and methyl esters.
Table 1  Literature studies investigating the performance and emission characteristics of ethyl esters in comparison with those of methyl esters based on the same feedstock by using different diesel engines

| Ref. | Biodiesel feedstock | Biodiesel percent (vol.%) in the biodiesel-diesel blend | Specifications of the tested engine | Test conditions | Properties | Performance | Emission |
|------|---------------------|--------------------------------------------------------|-----------------------------------|----------------|------------|-------------|----------|
|      |                     |                                                        |                                   |                | $\rho$ (kg/m$^3$) | $\mu$ (mm$^2$/s) | CV (MJ/kg) | BSFC (kg/ kWh) | BTE (%) | NO$_x$ (ppm) | HC (ppm) | PM (HSU) | CO (vol. % or ppm) |
| [30] | WFO                | 100%                                                   | 6-cylinder, TC, CR = 16.4:1, RP = 136 kW | Fixed engine load, various engine speeds | $\rightarrow$ | $\uparrow$ | $\uparrow$ | $\downarrow$ | $\uparrow$ | $\rightarrow$ | $\downarrow$ | N/A | ↓ |
| [31] | WFO                | 100%                                                   | 4-cylinder, TC, CR = 18.45:1, RP = 77 kW | Various engine speeds and loads | $\rightarrow$ | $\uparrow$ | $\uparrow$ | $\rightarrow$ | $\rightarrow$ | N/A | N/A | N/A | N/A |
| [32] | Jatropha Oil       | 20%                                                    | 1-cylinder, NA, CR = 17.5:1, RP = 7.4 kW | Variable engine loads | $\downarrow$ | $\uparrow$ | $\uparrow$ | $\uparrow$ | $\downarrow$ | $\rightarrow$ | $\rightarrow$ | $\rightarrow$ | $\rightarrow$ |
| [33] | Pongamia Oil       | 100%                                                   | 1-cylinder, RP = 5.2 kW | Variable loads and fixed engine speed | $\rightarrow$ | $\downarrow$ | $\uparrow$ | N/A | $\rightarrow$ | $\downarrow$ | N/A | $\uparrow$ | N/A |
| [34] | Jatropha Oil       | 5% 10%                                                 | 1-cylinder, CR = 17.5:1, RP = 5.9 kW | Variable engine loads | N/A | N/A | N/A | $\rightarrow$ | $\rightarrow$ | $\downarrow$ | $\rightarrow$ | $\rightarrow$ | $\rightarrow$ |
| [35] | 1-Soybean oil      | 20%                                                    | 4-cylinder, RP = 106 kW, V = 4.4 L | Variable engine loads | N/A | N/A | N/A | N/A | N/A | $\uparrow$ | N/A | N/A | N/A |
| [36] | Mesua Ferrea oil   | 10% 20%                                                | 1-cylinder, CR = 12–18, RP = 5.878 kW | Variable loads and compression ratios | $\downarrow$ | $\downarrow$ | $\rightarrow$ | $\downarrow$ | $\uparrow$ | $\downarrow$ | $\rightarrow$ | N/A | $\uparrow$ |
| [37] | Rapeseed oil       | 100%                                                   | 1-cylinder, CR = 17.5:1, RP = 5.5 kW | Various engine speeds | $\uparrow$ | $\uparrow$ | N/A | $\uparrow$ | N/A | $\rightarrow$ | $\rightarrow$ | $\rightarrow$ | $\rightarrow$ |
| [38] | Rapeseed oil       | 25% 50% 75% 100%                                       | Direct injection 4-cylinder Audi 80 engine | N/A | N/A | N/A | N/A | N/A | N/A | N/A | N/A | N/A | N/A |

Abbreviations and symbols: $\rho$, density; $\mu$, viscosity; CV, calorific value; BSFC, brake specific fuel consumption; BTE, brake thermal efficiency; NO$_x$, nitric oxide; HC, hydrocarbon; PM, particulate matter; CO, carbon monoxide; WFO, waste frying oil; TC, turbocharged; NA, naturally aspirated; V, volume of the engine; 100%, pure biodiesel; $\uparrow$, increase relative to methyl ester; $\downarrow$, decrease relative to methyl ester; $\rightarrow$, similarity with methyl ester; N/A, no data available
In compression ignition engines, fuel is directly injected via an injector into a chamber where the combustion of the fuel takes place. Hence, fuel atomization has a critical role in performance output and pollutant emissions. Fuel properties have a direct influence on spray characteristics. Biodiesel fuels generally have larger density, viscosity and surface tension values than petroleum-based diesel; this leads to higher spray penetration lengths, narrower spray cone angle values and larger droplet sizes [39–43]. Moreover, operating conditions strongly affect the spray characteristics, like fuel properties. Many research findings showed that spray cone angle widens, and spray penetration length reduces as the ambient pressure increases [40, 44]. Injection pressure is also an important operational parameter. Numerous research studies [43, 45, 46] showed that a rise in injection pressure increases the spray penetration length and spray cone angle, while some studies [44, 47, 48] reported that spray cone angle is insensitive to injection pressure. Besides, ambient temperature, nozzle diameter and combustion chamber design are other parameters affecting the spray characteristics [49, 50].

Since biodiesels are different compared to petroleum-based diesel fuels in density, viscosity and surface tension [51, 52], they can be further investigated in terms of their spray behaviour. Hence, it is important to perform research on the macroscopic and microscopic spray characteristics of alternative diesel fuels to figure out the effects of those fuels on the spraying process. Numerous studies concerning spray investigation of biodiesel fuels can be found in the literature [39–41, 50, 53]. However, all available literature studies have focused on spray patterns of methyl esters, which were produced via the utilization of fossil-based methanol in the transesterification process. Despite the importance of research focusing on spray characteristics, investigation on spray characteristics of ethyl ester type biodiesel fuels, to our best knowledge, is not yet available in the literature. Hence, this study intends to fill this important gap in the literature by investigating the spray characteristics, i.e. spray penetration length, spray cone angle and Sauter mean diameter of ethyl ester type biodiesel fuels derived from corn and sunflower oils in comparison to those of methyl esters based on the same feedstocks, and also of petrodiesel.

2 Experimental

2.1 Biodiesel production

Transesterification is a process that replaces the organic group of an ester with the organic group of alcohol, as shown in Fig. 1. For the production of biodiesel, 1 mol of triacylglycerol stoichiometrically reacts with 3 mol of alcohol in the presence of catalysts such as NaOH, KOH, etc., whereas, excess amount of alcohol is generally used to increase the biodiesel yield [54]. Biodiesel fuels tested in this study were produced from corn and sunflower oils (Kucukbay Oil and Detergent Inc. Trademark: Orkide). Against 1 mol of oil, 6 mol of methanol (to produce methyl ester) [55] and 24 mol of ethanol (to produce ethyl ester) [22] were used. Produced samples were referred to as CORME (corn oil methyl ester), SUNME (sunflower oil methyl ester), COREE (corn oil ethyl ester) and SUNEE (sunflower oil ethyl ester). All samples were produced at the Renewable Energy and Hydrogen Research Laboratory of İzmir Institute of Technology.

In this work, KOH was used as the catalyst. For the production of methyl and ethyl esters, catalyst-to-lipid ratios of 1 wt.% and 0.1 wt.% were respectively used. Apart from the alcohol and catalyst ratios used, the method, which is explained below, used for the production of both methyl and ethyl esters, was not changed. Reaction conditions are given in Table 2.

Transesterification procedures were started by preparing a catalyst-alcohol solution at room temperature. This solution was stirred at 1100 rpm while it was being heated up to 50 °C (WiseStir MSH-20D, temperature uncertainty ± 0.3 °C). When the temperature of the solution reached 50 °C, it was stirred for an additional 10 min at the same stirring rate. In this study, KOH was used as the catalyst. For the production of methyl and ethyl esters, catalyst-to-lipid ratios of 1 wt.% and 0.1 wt.% were respectively used. Apart from the alcohol and catalyst ratios used, the method, which is explained below, used for the production of both methyl and ethyl esters, was not changed. Reaction conditions are given in Table 2.

Table 2 Reaction conditions for the transesterification process

| Parameter                        | Methyl ester | Ethyl ester |
|----------------------------------|--------------|-------------|
| Type of alcohol                  | Methanol     | Ethanol     |
| Alcohol/lipid ratio              | 6:1          | 24:1        |
| Catalyst                         | KOH          | KOH         |
| Catalyst/lipid ratio             | 1 wt.%       | 0.1 wt.%    |
| Reaction temperature [°C]        | 50           | 50          |
| Reaction duration [h]             | 4            | 4           |

![Fig. 1 Biodiesel production through transesterification process](image)
the meantime, vegetable oil of which the biodiesel would be produced was heated to 50 °C. Transesterification reaction was begun by adding vegetable oil into the alcohol-catalyst solution. The alcohol-vegetable oil mixture was stirred at 1100 rpm for 4 h. After 4 h, the reaction was completed, and the mixture was left for glycerol precipitation. Glycerol precipitated in 4 h and was accordingly separated from the biodiesel. Next, the washing process was applied to remove the impurities from the biodiesel. Washing of biodiesel was performed with 5 vol.% acetic acid solution in water with a determined pH which was 2.48. The acetic acid solution was added to the biodiesel in a ratio of 1/3 vol/vol. Then, the acetic acid-biodiesel mixture was stirred for 1 h at a stirring speed of 500 rpm. After 1 h, the acetic acid solution was separated from biodiesel. The washing step was repeated until the pH value of the acetic acid solution, which was removed from the biodiesel-acetic acid mixture, becomes the same as the pH value of the neat acetic acid solution. In the following step, biodiesel was subjected to a vacuum evaporation process for 24 h at a temperature of 75 °C. In this way, the remaining water molecules could be removed from the biodiesel. After vacuum evaporation, biodiesel was ready for use.

2.2 Materials and fuel properties

In this work, Shell V-Power Diesel having a product code of 002D2609 (Shell & Turcas Petrol) was used as the reference fuel. More information is available in the diesel fuel data sheet [56].

The density values of diesel and biodiesel fuels were measured with a calibrated pycnometer at a temperature of 15 °C. The pycnometer had a volume of 25.066 ml with a sensitivity of 0.001 ml. AEK-Tech WT-1 thermometer (accuracy ± 1 °C, sensitivity 0.1 °C) was utilized to measure the temperature of the fuels during density measurements.

A AR 2000ex rheometer of TA Instruments was utilized to measure the viscosity of the fuels. Measurements were performed in controlled rate mode with an angular velocity of 10.5 rad/s as the input for rotating plates of the rheometer. All measurements were made for fuel temperatures of 40 °C. In addition, 60 data were collected with a sampling rate of 5 for each viscosity measurement of each fuel at the specified conditions in order to ensure the accuracy of the measurements. Viscosity values of the fuels reached steady-state values during obtaining 60 data. After reaching steady state, the values did not change with respect to time anymore. The viscosity values stated in Table 3 are the steady-state values.

In order to predict the surface tension effects of the fuels, contact angle values of all fuels were measured with glass at room temperature. Theta Optical Tensiometer (Attension), which had an accuracy of ± 0.1°, was used to measure the contact angle values.

The physical properties of the fuels are presented in Table 3. Besides, viscosity and density values of ethyl ester type biodiesel fuels were compared with the tested ethyl ester type biodiesel fuels based on different feedstocks in literature studies. This comparison is presented in Fig. 2, where the density and viscosity values of ethyl esters produced from various sources differ 1.6% and 22.1% on average, respectively.

As can be seen in Table 3, the physical properties of biodiesel fuels differ from those of the reference petrodiesel. Density, viscosity and contact angle values of both methyl and ethyl esters were higher than those of diesel. CORME and SUNME respectively had higher densities by 6.5% and 6.2%; higher viscosities by 1.9 and 1.7 times and larger contact angle values by 39.1% and 38.3% than fossil diesel. Density values of COREE and SUNEE were respectively 5.3% and 4.4% higher than the density of diesel. The viscosity of COREE and SUNEE was 2.2 and 1.9 times higher than that of conventional diesel while the contact angle values of COREE and SUNEE were 35.8% and 34.5% larger.

The physical properties of ethyl esters can be compared with that of methyl esters’ produced from the same

| Test fuel                  | Diesel | CORME | SUNME | COREE | SUNEE |
|----------------------------|--------|-------|-------|-------|-------|
| Viscosity (mm²/s) @ 40 °C  | 3.07   | 5.83  | 5.17  | 6.67  | 5.85  |
| Density (kg/m³) @ 15 °C    | 829.55 | 883.26| 880.83| 873.69| 865.71|
| Contact angle (°) with glass @ 25 °C | 14.71 | 20.46 | 20.34 | 19.98 | 19.78 |

Fig. 2 Comparison of physical properties of ethyl esters with literature studies [30, 32, 33, 35, 37, 57]
feedstock. Although physical properties of biodiesels vary limitedly among themselves, ethyl esters had lower density and contact angle values than that methyl esters; on the contrary, their viscosity values were higher than those of methyl esters. COREE had 1.1% lower density, 1.1 times bigger viscosity and 2.4% decreased contact angle values than CORME. The density of SUNEE was 1.7% lower than the density of SUNME. The viscosity value of SUNEE was 1.1 times bigger than that of SUNME. SUNEE had a 2.8% reduced contact angle value than SUNME.

2.3 Experimental setup

Fuel spray experiments were conducted in a bench-scale spray test setup (Fig. 3) consisting of a constant volume chamber (CVC) and with fuel injection, gas filling, optical and control systems. The setup allows reactive and non-reactive spray measurement. In this work, the target was observing the influence of the physical properties of ethyl ester on the spray characteristics, rather than its methanol counterpart (i.e. methyl ester). Hence, only a non-reactive spray study was carried out. A non-reactive environment can be achieved by adding nitrogen gas into the chamber.

To inject the test fuels into the chamber a fuel injection system was employed in the test setup. The injector, common rail, fuel pump, fuel filter and fuel tank are the components of the fuel injection system. A Siemens brand diesel injector with originally 7 holes of which 6 holes were closed by laser welding was used. In this way, it was possible to focus on the formation of only one spray.

The setup allows the identification of the liquid phase of fuel sprays via an optical system based on the shadowgraph method (Fig. 3). The chamber was established with quartz windows allowing optical accessibility. The spray visualization system consists of 7 components such as optical table, high-speed camera, a convex lens, parabolic mirror, off-axis mirror mount, light source and diaphragm. Table 4 gives information about the equipment employed in the optical setup. Furthermore, the high-speed camera was utilized to record an injection event at 20,000 fps, shutter speed of 1/62,000 with a resolution of 512 × 512 pixels during the experiments.

A control system is responsible for controlling the equipment, receiving and transmitting the data. This system consists of a computer, National Instruments (NI) USB 6343 and USB 6353 data acquisition (DAQ) cards. A control programme was prepared in LabVIEW software to process the data, and to give necessary commands. Mainly, the control system can amplify the signal going to the motor of the fuel pump via motor drivers, adjust the fuel injection pressure, start and stop injection event and start and stop image recording. Besides, the control system can measure and control the chamber pressure and temperature with the equipment listed in Table 5.

Total uncertainty (u) of the experiments can be found by taking the square root of the sum of squares of uncertainty.
values for measurement devices [58], which are listed in Table 5. Total uncertainty for this study was calculated as ± 0.84%.

### 2.4 Test conditions

Experiments were conducted under variable chamber pressures of 0, 5, 10 and 15 bar, and variable injection pressures of 600 and 800 bar, while the chamber was kept constant at room temperature. The injection pressures were utilized since the fuel pump is not stable at higher injection pressures. An installed experimental setup can achieve these pressure values. In addition, fuel impingement to the chamber wall could occur at higher injection pressures, e.g. 1200–1800 bar. At these pressures, it might be difficult to distinguish the spray characteristics of different fuels. Moreover, the values for the chamber pressure were selected to observe the mixing effect of air because air viscosity varies with the pressure. Besides, injection duration was kept at 1 ms. Table 6 shows the test conditions, which were selected based on existing literature [39, 43, 44, 48, 52, 53].

Tests were repeated five times for all test conditions to ensure the accuracy of the study. Mean values of the experiments were calculated, and it was observed that the deviation of the experimental results from the mean values, which was named repeatability, did not exceed 5%. The results were presented as the mean values of the tests corresponding to each experimental condition. Besides, uncertainty values for the experiments were already given as ± 0.84%. Repeatability bars are shown on the graphs in the results section. Because the uncertainty value was smaller than the repeatability value, uncertainty bars were not included in the graphs.

### 2.5 Image processing

SPL is the length between the furthest point of the spray on its axis and the nozzle of the injector. SCA can be defined as the angle between the tip of the injector and the two outermost points on the spray boundary. SCA can be measured from the points corresponding to 50% of the spray length according to the literature [44, 59, 60]. The spray images were recorded by a high-speed camera during the experiments. These images were then processed in order to measure spray characteristics, accurately. ImageJ [61] and MATLAB were utilized for image processing. Procedures for image processing are presented in Fig. 4. First of all, spray images were subjected to background subtraction so that only the spray shape remained. The recording of the

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**Table 4** The list of equipment in the optical system

| Component                  | Model and/or property                                                                 |
|----------------------------|---------------------------------------------------------------------------------------|
| Optical table              | 600 × 1200 mm metric optical table                                                    |
| Light source               | Edmund Optics MI-150 fibre light source, 150 W quartz halogen                          |
| Diaphragm                  | Diameter of 30.8 mm, aperture: 0.8–12 mm                                              |
| Mirror mount               | Parabolic mirror mount with a diameter of 101.6 mm                                     |
| Off-axis parabolic mirror  | Edmund Optics 101.6 × 152.4 mm EFL 90° protected aluminium 100A off-axis parabolic mirror |
| Convex lens                | Diameter: 125 mm, focal length: 250 mm                                                |
| High-speed camera          | Photron SA 1.1 with a Sigma lens (Sigma 24–70 mm f/1:2.8)                              |

**Table 5** Measurement devices employed in the spray test rig

| Equipment                       | Parameter                  | Range (Units) | Accuracy |
|---------------------------------|----------------------------|---------------|----------|
| MAX6675 K-type thermocouple     | Temperature                | −20–80 °C     | 0.25%    |
| Emko ESM-4420 temperature control device | Temperature              | 0–50 °C       | 0.25%    |
| Kistler 4075A50V200S pressure sensor | Pressure                 | 0–50 (bar)    | 0.1%     |
| Kistler Piezoresistive amplifier type 4624A (for pressure measurement) | Voltage output             | 0–10 (V)     | 0.05%    |
|                                | Error of the electronics   |                | 0.75%    |

**Table 6** Experimental conditions

| Condition                           | Property                        |
|-------------------------------------|---------------------------------|
| Injector type                       | Piezoelectric common rail injector |
| Number of the nozzle holes           | 1                               |
| Injection angle into the chamber w.r.t. horizontal axis | 45° (clockwise direction) |
| Chamber temperature                 | 25 °C                           |
| Chamber pressure (absolute)         | 0, 5, 10, 15 bar                |
| Injection pressure                  | 600, 800 bar                    |
| Injection duration                  | 1 ms                            |
| Repetition of the experiments       | 5 times for each test condition |

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spray images took place simultaneously with the initiation of the injection process. The image recording started 4 frames before the spray operation so the background image of the spray process was obtained. This background was then subtracted from each spray image, and images containing only fuel spray were obtained. Images from step one were converted to binary images by applying thresholding. The threshold value was calculated using Otsu’s method [62], and this value corresponded to 0.4. In the third step, boundaries of the spray images were detected and spray penetration lengths were measured. After obtaining the SPL values, lengths corresponding to 50% of the spray penetration lengths (0.5*SPL values) were calculated, and spray cone angles were measured by considering the 0.5*SPL values.

### 3 Results and discussions

All fuels including methyl esters, ethyl esters and fossil diesel fuel showed similar macroscopic spray shapes with minor differences under the variable chamber and injection pressures. Increasing the ambient pressure reduced the spray penetration lengths (Figs. 5 and 6), on the other hand, widened the spray cone angles for all fuels (Figs. 7 and 8). Increasing the chamber pressure raised the gas density in the chamber. This led to more resistance to spray at the tip and decreased spray propagation in the spray axis significantly. Continuous mass flow from the injector during the injection process caused the spray to spread in the radial direction because of the inhibited penetration in the axial direction, which resulted in an enlarged spray angle [44]. This result is consistent with the study by Lee et al. [40]. They explained that increased ambient pressure led to enlarged spray angles and a longer time to reach a specified spray penetration length. Besides, increasing the injection pressure increased the penetration lengths (Fig. 6) while keeping the spray cone angles almost unchanged (Fig. 8). Increasing the injection pressure raised the kinetic energy of the spray, which enhanced the spray process in the axial direction as well as the radial direction. But, the growth in the axial direction was remarkably quicker than it was along the radial direction [44]. Therefore, spray tip penetration increased while rising the injection pressure on the contrary no change occurred in the spray cone angle under the given experimental conditions. Wang et al. [47] also observed an increase in the spray penetration length while spray cone angle values remained almost constant with raise in fuel injection pressure.

Besides, the chamber pressure was found to be more effective on spray characteristics than fuel injection pressure. For example, spray penetration lengths of diesel at zero chamber pressure at 0.4 ms of the injection were approximately 91.2 mm and 102.4 mm for injection pressures of 600 and 800 bar, respectively. The difference was approximately 11.2 mm. Spray cone angle values under the same conditions were respectively found to be as 8.2° and 8.4° for injection pressures of 600 and 800 bar. From another point of view, penetration lengths of diesel fuel at an injection pressure of 600 bar at the same instant of the injection were approximately 91.2 mm and 46.5 mm for...
ambient pressures of 0 and 5 bar. To be specific, the difference was 44.7 mm. Under the same conditions, spray cone angle values were respectively measured as 8.2° and 14.8°. Namely, the spray cone angle widened 6.6° with an increase in ambient pressure. Eventually, these values showed that chamber pressure was more effective on spray characteristics than injection pressure in these experimental conditions. This result is consistent with the result found by He et al. [63]. They reported that the effect of ambient pressure on spray characteristics was stronger than that of fuel injection pressure.

In addition, the difference between spray penetration lengths at injection pressures of 600 bar and 800 bar decreased as the pressure inside the chamber increased as shown in Fig. 9. For instance, this difference was found as 7.8 mm for COREE at 0.8 ms of the injection when chamber pressure was 5 bar. However, this difference decreased to 3.3 mm and 1.3 mm when the ambient pressure was respectively increased to 10 and 15 bar. Namely, increasing the chamber pressure reduced the effects of increasing the injection pressure.

On the one hand, higher injection pressures (even larger injection pressures than the pressures used in this study) may
be beneficial due to the possible improvement in atomization as demonstrated in this study. The primary breakup of the fuel jet starts soon after leaving the injector nozzle and large droplets form near the nozzle. The main driving mechanisms for the primary breakup are cavitation and turbulence in case the injection pressure is high \[64\]. Then, existing droplets break up into smaller ones. This process is called secondary breakup and mainly occurred by the relative velocity between the fuel droplets and the air \[65\].

Increasing the injection pressures raises the fuel velocity resulting in a larger \( \text{Re} \) number, which is presented in the following equation:

\[
\text{Re} = \frac{u D \rho_l}{\mu_l} \quad (1)
\]

where \( \mu_l \) is the fuel viscosity, \( \rho_l \) is fuel density, \( D \) is the nozzle diameter and \( u \) is the jet velocity. It can be expected that
the fuel droplets should get more inertia against breakup leading to increased droplet diameter, based on raised Re number. However, when the injection pressure increases, the relative velocity between the fuel droplets and the almost stagnant air also increases. This air drag manifests itself as a fluctuating pressure and shear on the fuel droplet due to the high Re number. Therefore, an improvement in a secondary breakup can be expected, and the larger droplets disintegrate into smaller ones. Then, decreased droplet sizes can be achieved as a result of secondary breakup caused by high injection pressure [65]. Besides, Yadav and Gautam [66] explained that utilizing high injection pressures can reduce the rheological properties of fuels such as its surface tension. In case of variation in fuel velocity and fuel properties as a result of high injection pressures, Re number would change as well as Ohnesorge number (Z). Z is a dimensionless number to define the jet breakup regimes, which includes all relevant properties of fuel, as shown in Eq. (2) [65]:

![Fig. 7 (a, b) Spray cone angle (SCA) values for ethyl esters under variable injection pressures in comparison to those of diesel and methyl esters](image)
where $\sigma$ is the surface tension of a fuel. Re number increases due to the increase in inertial effects more than viscous effects. $Z$ number may also rise owing to possible slight changes in rheological properties. Thence, fuel atomization is enhanced. This is supported by the previous explanation regarding the second breakup as a consequence of an increase in injection pressure. On the other hand, this is an issue that needs attention. Very high injection pressures can have the possibility of wall impingement in diesel engines causing an increase in fuel consumption as well as HC and PM emissions [66, 67].

Furthermore, spray penetration curves could be divided into two phases which were the rapid development phase and steady development phase. Spray penetration length rapidly increased in the rapid development phase then passed to the steady development phase in which spray penetration steadily increased and reached the maximum value. Besides,
differences between the biodiesels and fossil diesel occurred in the steady development phase while similar penetrations were observed in the rapid development phase. This is consistent with the literature [68, 69]. Also, spray cone angle curves could be divided into two phases: the transient and the steady phases. Besides, these regions are related to the needle valve of the injector [68, 69]. In the transient phase, the needle valve was partially open, and radial momentum was high. These caused the spray cone angle to increase abruptly. In the steady phase, the needle valve was fully open, and radial momentum decreased. Then, the spray cone angle reduced and became almost constant.

At zero chamber pressure, no significant distinctions between ethyl esters and reference diesel fuel were found under both injection pressures when the uncertainty and repeatability values are taken into account as it is seen in Figs. 6a and 8a. All fuels impinged to the wall of the chamber by penetrating fast during the first 0.5 ms of the injection process.

When the ambient pressure was increased to 5 bar, pronounced differences were observed between diesel and ethyl esters in terms of spray penetration length and spray cone angle (see Figs. 6b and 8b). Ethyl esters had larger spray penetration length and reduced spray cone angle values than reference diesel fuel. For instance, COREE could be compared with diesel under an injection pressure of 600 bar at 0.8 ms of the injection duration. Spray penetration lengths were respectively measured as 88.7 and 78.3 mm for COREE and diesel. Spray cone angle values were found to be 13.2° and 25.6° for COREE and diesel, respectively. In addition, spray wall impingement was observed for biodiesel fuels at the end of the injection process for both injection pressures of 600 and 800 bar. However, diesel fuel did not impinge to the chamber wall.

When the chamber pressure was further raised to 10 bar, any fuel did not impinge to the wall. Moreover, the difference between spray characteristics of ethyl esters and fossil diesel decreased while ethyl esters still had higher spray penetration lengths and narrower spray cone angle values as shown in Figs. 6c and 8c. For example, SUNEE had a spray cone angle of 17.5° and spray penetration length of 54.1 mm at 0.6 ms of the injection under an injection pressure of 800 bar. Under the same conditions, spray penetration length and spray cone angle values of diesel were respectively measured as 52.4 mm and 16.7°.

Hereby, it can be stated that fuel properties directly affect the spray characteristics. Ethyl esters had longer spray penetration lengths and narrower spray cone angle values under chamber pressures of 5 and 10 bar for injection pressures of 600 and 800 bar. These results can be explained with higher contact angle, density and viscosity values of ethyl esters than diesel. Having higher contact angle values shows that surface tension effects of ethyl esters are greater than fossil diesel leading to decreased disintegration of spray resulting in narrower spray angles and increased liquid lengths [39]. Also, viscosity is effective for spray characteristics. Because, higher viscosity reduces the fuel atomization leading to narrower spray angles and deeper spray penetration lengths [41]. In addition, higher density values can increase the momentum of fuel spray thus extends the penetration lengths [43].

At the chamber pressure of 15 bar, the difference between diesel and ethyl esters further reduced in terms of both spray penetration length and spray cone angle (Figs. 6d and 8d). At this pressure level, the differences between ethyl esters and reference diesel were so small that can be neglected. For instance, the distinction between spray cone angle values of COREE and conventional diesel were measured as 0.4° at the end of the injection duration under injection pressure of 800 bar. At the same conditions, the difference between diesel and COREE in terms of spray penetration length was found to be 1 mm. When considering the uncertainty and repeatability, these differences have no point.

Moreover, it can be stated that the difference between ethyl esters and the petrodiesel decreased in terms of both spray characteristics as the chamber pressure increased. At zero chamber pressure, it was explained that diesel and ethyl esters had very similar spray characteristics because there was no air inside the chamber leading to neither turbulent mixing nor shear drag. This might explain the lack of distinction between diesel and ethyl esters. However, the situation was different when there was pressure inside the chamber, especially at 5 bar. Kinematic viscosity of air decreases as the density of the air inside the chamber increases. Reduced kinematic viscosity of air could improve the mixing of fuel-air because the air becomes more prone to turbulence as its kinematic viscosity gets smaller. Hence, air turbulence around the fuel spray may lead to the disintegration of the fuel spray. Since the surface tension effects of fossil diesel fuel were lower than ethyl esters, the air mixed the diesel
fuel more than ethyl esters leading to wider spray cone angles and reduced spray lengths when the ambient pressure was 5 bar. But, the kinematic viscosity of air became smaller when the ambient pressure was further raised. Thence, ethyl esters could be effectively mixed with air as similar as the reference diesel mixes with air due to the higher air turbulence at higher air densities. This may explain the reduction in differences of spray characteristics for ethyl esters and diesel as the ambient pressure increased and the similarity between diesel and ethyl esters at 15 bar ambient pressure.

When comparing the spray parameters of ethyl esters with methyl esters, a similarity was observed. For example, spray penetration lengths at 0.6 ms of the injection for CORME and COREE were respectively measured as 71.4 mm and 71.9 mm at an injection pressure of 600 bar under chamber pressure of 5 bar. As another example, penetration lengths of SUNME and SUNEE were respectively found as 71.7 mm and 71.8 mm under the same conditions. Besides, this likeness was observed for spray cone angle curves of both types of fuels. For instance, spray angles of CORME and COREE were respectively measured as 16.9° and 17.1° at 0.8 ms of injection under chamber pressure of 10 bar and injection pressure of 600 bar. As another example, SUNME and SUNEE had respectively spray angles of 12.9° and 12.7° at 0.2 ms of injection under an injection pressure of 800 bar and a chamber pressure of 5 bar. These similarities can be explained with the density, viscosity and contact angle values. The ethyl esters had larger viscosity values than the methyl esters nevertheless the methyl esters had bigger density and contact angle (and surface tension) values than the ethyl esters. These properties may have compensated each other and may have prevented differences in spray properties to occur. Moreover, the curves obtained for both ethyl esters and methyl esters were similar in macroscopic shape. One of the most important points was that effects of chamber pressure and injection pressure were similar for the two kinds of fuels. This may be because methyl esters and ethyl esters are the same in terms of the feedstock and production method thus, they are not physically completely different. Indeed, there were no huge distinctions in viscosity, contact angle and density values despite differences as explained in Section 2.2.

Sauter mean diameter (SMD) was calculated to estimate the microscopic spray characteristics of ethyl esters in comparison to those of methyl esters and fossil diesel. SMD is the average particle size of fuel droplets and can be calculated using the following correlation [47]:

$$\text{SMD} = 6156v^{0.385} \sigma^{0.737} \rho_f^{0.737} \rho_a^{0.06} \Delta P^{-0.54}$$  \(3\)

where \(v\) is the kinematic viscosity of a fuel, \(\sigma\) is the surface tension of fuel, \(\rho_f\) is fuel density, \(\rho_a\) is the air density and \(\Delta P\) is the pressure difference between the injection pressure and the ambient pressure.

The correlation contains surface tension term. In this work, the surface tension of test fuels could not be measured, but a calculation was performed by using values available in the literature. Table 7 shows the surface tension values for both biodiesel and fossil-based diesel fuels obtained from the existing literature work. The estimation was performed by taking the mean of the reported values. The margin of error was calculated by considering the maximum and minimum surface tension values and the possible range for the SMD values was estimated accordingly.

Figure 10 shows the estimated SMD values for all test fuels under all experimental conditions. Injection and ambient pressures are effective parameters on SMD. As seen in the figure, SMD decreased as the injection pressure increased, and increased as the ambient pressure increased. This is consistent with the literature data [66, 67]. Biodiesel fuels had, on average, around 47% higher SMD values than that of fossil-based diesel. Besides, ethyl esters had approximately 4% larger SMD values than methyl ester counterparts under the assumed surface tension value. However, contact angle values of ethyl esters were 2.6% lower than those of methyl esters, meaning that the surface tension effects of ethyl esters were slightly lower than those of the methyl esters. Considering this, the real difference in SMD values of methyl esters and ethyl esters could be less than 4%.

### 4 Conclusions

The aim of the study was to investigate the spray characteristics of ethyl ester-type biodiesel fuels and to compare them with those of methyl esters and fossil-based diesel fuel. Experiments were conducted in a constant volume chamber under various injection pressures (600 and 800 bar) and various ambient pressures (0, 5, 10 and 15 bar). The
The physical properties of the fuels had a direct effect on spray characteristics. On average, ethyl esters performed 2.8–20.2% deeper penetrations and 5.1–19% narrower spray angles than conventional diesel fuel under chamber pressures of 5 and 10 bar. In addition, SMD values of ethyl esters were around 48% higher than diesel on average. Higher density, viscosity and contact angle values of ethyl esters led to poorer atomization and increased spray momentum. In contrast, the macroscopic spray characteristics of ethyl esters were very similar to those of reference diesel fuel at the ambient pressure of 15 bar. On average, the distinctions were under 2%. Considering the uncertainty and repeatability values, which were respectively ± 0.84% and ± 5%, the difference was not significant.

Ethyl esters performed similar spray penetrations and angles with methyl esters. The difference between the fuels in terms of spray parameters were in the range of 1–3% for all test conditions. Besides, average SMD values of ethyl esters were lower than 4% compared to those of methyl esters considering all the test conditions. When taking the uncertainty and repeatability values into account, it could be stated that ethyl esters performed approximate results to methyl esters in terms of spray characteristics. This may be explained by considering density, viscosity and contact angle values. Ethyl esters had higher viscosity values on the contrary they had smaller density and contact angle values. These properties may have compensated each other thus similar spray characteristics may have been observed.

This study revealed that the spray characteristics of ethyl esters were very similar to those of methyl esters. As a result, the use of ethanol instead of methanol in biodiesel production cannot be considered a major drawback for diesel engines. Therefore, ethyl esters could have the potential of being used instead of methyl esters in diesel engines with no or small modifications. This will lead to the utilization of completely renewable biodiesels with improved cold weather performances.

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Data availability The datasets generated during and/or analysed during the current study are not publicly available due to confidentiality but are available from the corresponding author on reasonable request.

Declarations

Conflict of interest The authors declare no competing interests.

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