BaCu$_3$O$_4$: High Temperature Magnetic Order in One-Dimensional S=1/2 Diamond-Chains

C. W. Rischau$^1$, B. Leridon$^1$, D. Colson$^2$, A. Forget$^2$ and P. Monod$^1$

$^1$Laboratoire de Physique et d’Etude des Matériaux, UMR8213- CNRS-ESPCI ParisTech-UPMC 10 rue Vauquelin, 75231 Paris Cedex 05, France

$^2$Service de Physique de l’Etat Condensé, Orme des Merisiers, IRAMIS, CEA-Saclay (CNRS URA 2464), 91191 Gif sur Yvette Cedex, France

∗ Corresponding author: brigitte.leridon@espci.fr

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The magnetic properties of the alkaline earth oxocuprate BaCu$_3$O$_4$ are investigated. We show that the characteristic Cu$_3$O$_4$ layers of this material can be described with diamond chains of antiferromagnetically coupled Cu 1/2 spins with only a weak coupling between two adjacent chains. These Cu$_3$O$_4$ layers seem to represent a so far unique system of weakly coupled one-dimensional magnetic objects where the local AF ordering of the Cu$^{2+}$ ions leads to an actual net magnetic moment of an isolated diamond chain. We demonstrate a magnetic transition at a high Néel temperature $T_N = 336$ K.

INTRODUCTION

Lamellar copper oxides have been extensively studied not only regarding high-critical-temperature ($T_c$) superconductivity, but also regarding low-dimensional quantum magnets. Cupric oxide (CuO) itself exhibits two antiferromagnetic (AF) transitions at Néel temperatures $T_{N1,N2} = 213, 230$ K denoting a strong superexchange energy (70 meV) of the Cu-O-Cu coupling [1]. Recently, Kimura et al. detected ferroelectricity in CuO for $T_{N1} < T < T_{N2}$ and thus identified CuO as an induced-multiferroic [2]. Cu-O is also the key component of high-$T_c$ cuprate superconductors like YBa$_2$Cu$_3$O$_{6–x}$ (YBCO), (La,Sr)$_2$CuO$_4$ or HgBa$_2$CuO$_{4+\delta}$, which are composed of CuO$_2$ layers. These materials exhibit an antiferromagnetic phase in the underdoped non-superconducting regime of the phase diagram, but some groups additionally reported the existence of a commensurate alternate magnetization - probably of orbital nature - in the Cu-O planes of YBCO and HgBa$_2$CuO$_{4+\delta}$ well in the doping range of superconductivity [3,4]. Another interesting family of lamellar copper oxides are the oxochlorides like Ba$_2$Cl$_2$Cu$_3$O$_4$ or Sr$_2$Cl$_2$Cu$_3$O$_4$ (2234 materials) which are composed of Cu$_3$O$_4$ planes interseeded with Ba and Cl layers. The magnetic structure of these Cu$_3$O$_4$ layers results in two AF ordering temperatures and has been the focus of extensive experimental and theoretical studies (see [5,6] and Refs therein).

Here we report on the magnetic properties of the alkaline earth oxocuprate BaCu$_3$O$_4$ which is composed of Cu$_3$O$_4$ layers [7,10] with a different structure than those of the 2234 materials, and, as will be demonstrated, very different magnetic properties. As a matter of fact, BaCu$_3$O$_4$ exists only as a parasitic phase in YBCO samples [8], or on thin films grown on top of a suitable, epitaxial perovskite buffer layer [11]. We therefore performed our measurements on YBCO polycrystalline samples and single crystals which were shown to contain BaCu$_3$O$_4$.

METHODS

The magnetization of thirteen polycrystalline and six single crystalline YBCO samples with various oxygen contents (see Tab. I) was investigated using a MPMS 5T SQUID magnetometer. The polycrystalline samples were prepared at the SPEC-CEA from three different batches of YBa$_2$Cu$_3$O$_x$ powder (batches A, B and C) by compacting the powder into cylinders of 6 mm diameter and 6 mm height and annealing them under appropriate N$_2$-O$_2$ mixtures in order to obtain the desired oxygen content. Four different disks of YBCO single crystals (batches D, E, F, G) with various oxygen contents were obtained from different sources and cut into cubes with an edge length of usually 5 mm. The oxygen content of the samples D1, D2, D3 was changed using a thermobalance. In the following, the magnetization M will be given in emu/mol and is normalized to the amount of YBCO in mol. Every measurement was started by a zero field-cooling (ZFC) of the sample. This was followed by a measurement during warming (FW) and cooling (FC) the sample under the same magnetic field. It should be noted that the magnetic irreversibility of the superconducting wire used for the fabrication of the magnetometers solenoid produces a small remanent magnetic field in the range of ±10 Oe. Prior to the measurements at low field, this remanent field was determined by calibration of the magnetometer with a Pd sample and the field corrected for the remanent field will be referred to as $H_{real}$.

RESULTS

Figure I depicts the magnetization of a $x = 6.43$ polycrystalline YBCO sample (C 6.43, see Tab. I) measured under a magnetic field of 34 Oe as a function of temperature in the range from 300 to 380 K. The FW magnetization $M_{FW}$ after a zero field-cooling increases linearly.
TABLE I. Overview of all YBCO samples with \( T_c \) being their critical temperature and \( T_t \) the temperature of the observed transition (n.d.: transition non-detectable).

| Polycrystalline samples | Single crystals |
|-------------------------|-----------------|
| Name                    | \( T_c \) [K]   | \( T_t \) [K] | Name | \( T_c \) [K] | \( T_t \) [K] |
| C 6.19                  | -               | 340 ± 4       | D1 | 6.35          | -             |
| C 6.28                  | -               | 338 ± 2       | E  | 6.55          | 45 ± 1        | 335 ± 2       |
| C 6.34                  | -               | 338 ± 1       | F  | 6.65          | 55 ± 1        | n.d.          |
| C 6.43                  | 31 ± 1          | 337 ± 1       | D2 | 6.66          | 55 ± 1        | 334 ± 2       |
| C 6.52                  | 55 ± 1          | 338 ± 3       | D3 | 6.70          | 70 ± 1        | n.d.          |
| B 6.53                  | 58 ± 1          | n.d.          | D3 | 7.0           | 86 ± 1        | n.d.          |
| B 6.56                  | 60 ± 1          | n.d.          |    |               |               |               |
| A 6.60                  | 61 ± 1          | n.d.          |    |               |               |               |
| A 6.68                  | 62 ± 1          | n.d.          |    |               |               |               |
| A 6.73                  | 68 ± 1          | n.d.          |    |               |               |               |
| C 6.79                  | 80 ± 1          | 338 ± 1       |    |               |               |               |
| C 6.90                  | 91 ± 1          | 337 ± 1       |    |               |               |               |
| C 7.0                   | 91 ± 1          | 338.6 ± 1     |    |               |               |               |

with increasing temperature up to \( T \approx 330 \) K followed by a second slightly shallower linear increase for \( T \geq 340 \) K. The FC magnetization \( M_{FC} \) exhibits a behavior similar to \( M_{FW} \) for \( T \geq 340 \) K, but then shows a visible increase of the magnetization at a temperature of \( T_t = (337 \pm 1) \) K. In order to investigate this transition quantitatively, we extrapolated the \( M(T) \) curve above the transition to 300 K and defined the difference of the FC magnetization at 300 K with respect to this extrapolation as the step height \( \Delta M \) of the transition. The step height \( \Delta M \) of the transition shown in Fig. 1 amounts to \((1.3 \pm 0.1) \times 10^{-3} \) emu/mol.

The inset of Fig. 1 depicts \( \Delta M \) as a function of the real applied field \( H_{real} \) for the same sample, i.e., the remanent magnetic field in the magnetometers solenoid has been taken into account for these measurements. At first, the step height \( \Delta M \) increases steeply with increasing magnetic field up to \( H_{real} = \pm 30 \) Oe and then saturates at \( \Delta M \approx \pm 1 \) emu/mol. Since the absolute value of the step height moves within the range of \( 10^{-6} \) emu, the transition could not be observed in high field measurements. The temperature of the transition \( T_t \) showed no dependence on the magnetic field up to 0.1 T and is given in Tab. II for each sample.

Figure 2 shows the magnetization of a \( x = 6.5 \) YBCO single crystal (E 6.5) as a function of temperature measured under a field of 50 Oe with \( \mathbf{H} \parallel \mathbf{c} \) parallel to the crystals \( \mathbf{c} \) axis. The \( M(T) \) behavior is dominated by a strong Curie-Weiss contribution of paramagnetic secondary phases such as the green phase \( \text{Y}_2\text{BaCuO}_5 \) [12], \( \text{BaCuO}_2 \) [12] and a Curie contribution from free Cu atoms in the Cu-chains of YBCO [13]. In addition, \( M_{FC} \) shows a visible transition at a temperature \( T_t = (332 \pm 2) \) K. The inset of Fig. 2 depicts the magnetization of the \( x = 6.5 \) single crystal (E 6.5) measured under a field of 50 Oe for three different orthogonal orientations of the crystal with respect to the magnetic field, clearly revealing the YBCO anisotropy of \( M(T) \) between the directions \( \mathbf{H} \parallel \mathbf{c} \) and \( \mathbf{H} \parallel \mathbf{ab} \). However, for all three orientations \( M_{FC} \) shows a visible transition at \( T_t = (332 \pm 2) \) K with step heights of \( \Delta M = (0.6 \pm 0.1) \times 10^{-2} \) emu/mol for \( \mathbf{H} \parallel \mathbf{c} \).
and $\mathbf{H} \perp \mathbf{c}$ #2 and $0.7 \pm 0.1 \times 10^{-2}$ emu/mol for $\mathbf{H} \perp \mathbf{c}$ #1, i.e., there seems to be no visible dependence of the step height on the orientation of the crystal with respect to the magnetic field.

We measured three different batches of polycrystalline YBCO samples and four different batches of single crystals with different oxygen contents $x$. The transition was only observed for one of the three batches of polycrystalline samples and two of the four batches of single crystals (see Tab. I), therefore ruling out the origin for the transition as intrinsic to YBCO. Neither the existence, nor the temperature of the transition did depend on the oxygen content between $x = 0.19$ to $x = 1.0$. (An extensive study about the effects of oxygen disorder on the superconducting and pseudogap properties of YBCO was performed and is described elsewhere [14].

The present transition temperature was shown to be independent of these effects to within our measurement accuracy.) The average temperature $T_i$ of all detected transitions amounts to $(336 \pm 3)$ K.

**DISCUSSION**

Impurity phases present in YBCO have been extensively studied. However, the average temperature of the observed transition of $(336 \pm 3)$ K does not match with any of the Néel or Curie temperatures of common impurity phases such as $\mathrm{Y}_2\mathrm{BaCuO}_5$ ($T_N = 30$ K [12]), $\mathrm{Y}_2\mathrm{Cu}_2\mathrm{O}_5$ ($T_N = 13$ K [13]), $\mathrm{BaCuO}_2$ ($T_N = 15$ K [10]) or $\mathrm{CuO}$ ($T_{N1,N2} = 213, 230$ K [11]). This suggests that the transition is either due to an unknown impurity phase or an impurity phase with unknown magnetic properties. As a matter of facts, we detected the presence of the alkaline earth oxocuprate $\mathrm{BaCu}_3\mathrm{O}_4$ in samples showing the magnetic transition at $(336 \pm 3)$ K using Raman spectroscopy [17,18]. The micro-Raman spectrum is displayed in Figure 3. $\mathrm{BaCu}_3\mathrm{O}_4$ was identified for the first time as a secondary phase in YBCO samples by Bertinotti et al. using X-ray diffraction (XRD) [9] and confirmed later [10]. Since $\mathrm{BaCu}_3\mathrm{O}_4$ is metastable and only grows epitaxially on YBCO or other perovskite structures, there are only few studies (among them Raman spectroscopy [17,18]) of this material and its magnetic properties are unknown. However, as pointed out in Ref. [9], the structure of $\mathrm{BaCu}_3\mathrm{O}_4$ is close to the structure of the stable materials $\mathrm{Ba}_2\mathrm{Cl}_2\mathrm{Cu}_3\mathrm{O}_4$ and $\mathrm{Sr}_2\mathrm{Cl}_2\mathrm{Cu}_3\mathrm{O}_4$ (2234 materials) which show a magnetic transition at $330$ K [7] and $380$ K [8], respectively. $\mathrm{BaCu}_3\mathrm{O}_4$ consists of Ba and $\mathrm{Cu}_3\mathrm{O}_4$ planes (see Fig. 1 (a)) whereas the lattices are composed of Ba (respectively Sr) planes, Cl planes and $\mathrm{Cu}_3\mathrm{O}_4$ planes. Fig. 1 depicts the $\mathrm{Cu}_2\mathrm{O}_2$ planes of YBCO (b) and the $\mathrm{Cu}_3\mathrm{O}_4$ planes of 2234 materials (c) and $\mathrm{BaCu}_3\mathrm{O}_4$ (d). The $\mathrm{Cu}_2\mathrm{O}_2$ layers of YBCO (see Fig. 1(b)) are composed of a square lattice with $\mathrm{Cu}^{2+}$ ions ($d^9$, $S=1/2$) on the corners ($\mathrm{Cu}_I$ sites) and O ions on the edges. Nearest neighbor (NN) $\mathrm{Cu}_I$ ions are coupled via superexchange interaction through the oxygen atom between them resulting in an antiferromagnetic (AF) order below 420 K for YBCO.

Regarding the similarities in the structure of the $\mathrm{Cu}_3\mathrm{O}_4$ planes, the magnetic properties of $\mathrm{BaCu}_3\mathrm{O}_4$ and 2234 materials are expected to bear some resemblances. The
Cu$_3$O$_4$ planes of 2234-materials (see Fig. 4 (c)) consist of the CuO$_2$ structure shown in Fig. 4 (b) with additional Cu ions at the center of every second square (Cu$_{III}$ sites). The Cu$_{I}$-O-Cu$_{I}$ coupling (superexchange energy $J_0 \approx 130$ meV) is similar to that described for the CuO$_2$ planes of YBCO and results in an AF order below $T_N \approx 330$ and 380 K for Ba$_2$Cl$_2$Cu$_3$O$_4$ [7] and Sr$_2$Cl$_2$Cu$_3$O$_4$ [8], respectively. The Cu$_{II}$-Cu$_{II}$ coupling is much weaker ($J_I \approx 10$ meV) and gives rise to an AF order below $T_N \approx 30$ and 40 K for Ba$_2$Cl$_2$Cu$_2$O$_4$ [5] and Sr$_2$Cl$_2$Cu$_2$O$_4$ [8], respectively, while no magnetic anomaly is observed in this range of temperature for our samples. Since the interaction of a Cu$_{II}$ ion with the four surrounding Cu$_I$ ions is frustrated, the Cu$_I$ and Cu$_{II}$ sublattices should be decoupled, except for quantum fluctuations [10]. The Cu$_{III}$O$_4$ planes of BaCu$_3$O$_4$ consist of Cu ions on two different sites, namely Cu$_I$ and Cu$_{III}$, and the lattice can be described with ”diamond chains” (marked in gray in Fig. 2 (d)) consisting of squares attached by their Cu$_I$ corner ions. Cu$_I$ are strongly coupled to their four next NN Cu$_{III}$ via 180° Cu$_I$-O-Cu$_{III}$ ($J_0$) superexchange interaction and only weakly coupled to their two NN Cu$_{III}$. Since the temperature of the observed transition $T_I = (336 \pm 3)$ K is close to $T_N^N$ of Ba$_2$Cu$_3$O$_4$Cl$_2$, we attribute $T_I$ to an AF order resulting from the 180° Cu$_I$-O-Cu$_{III}$ coupling. Unlike the Cu$_I$ and Cu$_{II}$ sublattices in 2234 materials, the Cu$_I$ and Cu$_{II}$ sublattices in BaCu$_3$O$_4$ are strongly coupled, resulting in a unique AF order temperature for all Cu ions. Another important difference with respect to the 2234 materials is that in BaCu$_3$O$_4$ the order is strictly one-dimensional and not two-dimensional. It is noteworthy that the net magnetization of a single diamond chain is not zero, but one Bohr magneton per three Cu ions since the cell pattern consists of three Cu ions, one bearing an opposite magnetization with respect to the two others. There remains the question of the relative ordering of two adjacent and weakly coupled diamond chains. As weak as this interchain coupling may be, it favors the existence of one-dimensional order, which is a key issue inasmuch as such Ising-type order is forbidden when only a pure superexchange mechanism is present (another favoring mechanism may also be the spin-orbit coupling). The first hypothesis for the relative ordering of two adjacent chains is illustrated in Fig. 5 (a) and assumes that two NN diamond chains have parallel magnetizations. This would result in a ferrimagnetic order and the net magnetization of one Cu$_{III}$O$_4$ layer would be $1/3\mu_B$ per Cu. In the case where all layers are similarly oriented, we can estimate the molar fraction of BaCu$_3$O$_4$ in our samples to about 2×10$^{-6}$, which is much too small to be detected by Raman or XRD spectroscopy and therefore not realistic.

A second hypothesis is that the chains have parallel magnetizations within one given layer but the layers are AF ordered. This could in principle give rise to metamagnetism with a ”spin-flop” transition at sufficiently high magnetic fields which was not observed up to 5T. The third hypothesis is that the magnetic order of two adjacent chains is antiparallel (see Fig. 5(b)), so that the net in-plane magnetization is zero at zero field and the resulting order within the planes is antiferromagnetic. In this case the observed magnetization can be due to the Dzyaloshinskii-Moriya (DM) interaction, which is allowed by symmetry (since the oxygen atom at the center of the Cu$_{I}$-O-Cu$_{III}$ bond does not bear a center of inversion symmetry) and produces a net out-of-plane moment, able to rotate around the Cu-O bond axis under a magnetic field. This hypothesis of weak ferromagnetism is in fact the only one to be consistent with our observation that the step height $\Delta M$ is of the same amplitude for all orientations of the crystal with respect to the magnetic field (see Fig. 2 (note that at zero field the DM contributions of two neighboring chains cancel out). If the third hypothesis is valid, then making the rough assumption that the magnetic step heights $\Delta M$ in 2234 materials and in BaCu$_3$O$_4$ are the same, the molar fraction of BaCu$_3$O$_4$ in our samples would be about 2×10$^{-3}$, therefore compatible with Raman observation. Through neutron scattering measurements on underdoped YBCO, Sidis et al. [20] reported coexistence of magnetism and superconductivity at the doping level $x = 6.5$. Part of the sample used for this study is our sample E 6.5 in which we detected BaCu$_3$O$_4$ through Raman spectrometry (see Figure 3). The above inferred concentration could also be compatible with the observation of a very small moment through neutron scattering, but too small to be detectable through muon-spin-resonance ($\mu$SR) [21]. Since BaCu$_3$O$_4$ grows epitaxially on YBCO, this also explains the commensurability of the reported magnetic order. This newly discovered magnetic transition in BaCu$_3$O$_4$ might then account for some cases of apparent coexistence of magnetism and superconductivity in underdoped YBCO.
From the theoretical point of view, according to the pioneering work of Takano and coworkers \cite{21} on the phase diagram of diamond chains, BaCu$_3$O$_4$ appears indeed to belong to the ferrimagnetic case, however chain interactions deserve further study.

**CONCLUSION**

We reported on the magnetic properties of BaCu$_3$O$_4$, a common parasitic phase in YBa$_2$Cu$_3$O$_x$ samples. The magnetic order that sets in at 336 K is most probably due to diamond chains of antiferromagnetically coupled Cu 1/2 spins. The measured magnetization may be attributed to either ferrimagnetic ordering or (most probably) antiferromagnetic ordering of adjacent chains in the presence of the Dzyaloshinsky-Moriya interaction yielding weak ferromagnetism behavior. These diamond chains represent a new remarkable system of weakly coupled one-dimensional magnetic objects where AF ordering of the Cu$^{2+}$ ions in each diamond chain leads to a net magnetic moment of each chain.

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