Degree-scale galactic radio emission at 122 MHz around the North Celestial Pole with LOFAR-AARTFAAC

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ABSTRACT

Aims. Contamination from bright diffuse Galactic thermal and non-thermal radio emission poses crucial challenges in experiments aiming to measure the 21-cm signal of neutral hydrogen from the cosmic dawn (CD) and Epoch of Reionisation (EoR). If not included in calibration, this diffuse emission can severely impact the analysis and signal extraction in 21-cm experiments. We examine large-scale diffuse Galactic emission at 122 MHz around the North Celestial Pole, using the Amsterdam-ASTRON Radio Transient Facility and Analysis Centre (AARTFAAC)- High Band Antenna (HBA) system.

Methods. In this pilot project, we present the first-ever wide-field image produced with a single sub-band of the data recorded with the AARTFAAC-HBA system. We demonstrate two methods, multi-scale CLEAN and shapelet decomposition, to model the diffuse emission revealed in the image. We used angular power spectrum metrics to quantify different components of the emission and compared the performance of the two diffuse structure modelling approaches.

Results. We observed that the point sources dominate the angular power spectrum \((\ell(\ell + 1)C_{\ell}/2\pi \equiv \Delta^2(\ell))\) of the emission in the field on scales of \(\ell \gtrsim 60\) (\(\lesssim 3\) degree). The angular power spectrum after subtraction of compact sources is flat within the \(20 \lesssim \ell \lesssim 200\) range, suggesting that the residual power is dominated by the diffuse emission on scales of \(\ell \lesssim 200\). The residual diffuse emission has a brightness temperature variance of \(\Delta C_{\ell=180} = (145.64 \pm 13.61) K^2\) at 122 MHz on angular scales of 1 degree, and it is consistent with a power law following \(C_{\ell} \propto \ell^{-2.9}\) in the \(20 \lesssim \ell \lesssim 200\) range. We also find that, in the current set-up, multi-scale CLEAN is suitable to model the compact and diffuse structures on a wide range of angular scales, whereas the shapelet decomposition method better models the large scales, which are of the order of a few degrees and wider.

Key words. dark ages, reionization, first stars – methods: observational – methods: statistical – techniques: interferometric – radio continuum: general – radio continuum: ISM

1. Introduction

Observations of the redshifted 21-cm hyperfine transition line of neutral hydrogen (HI hereafter) are expected to unveil the properties of the first luminous objects and the evolution of the large-scale structure during the dark ages (CD; 12 \(\lesssim z \lesssim 30\)) and Epoch of Reionisation (EoR; 6 \(\lesssim z \lesssim 12\)) (Madau et al. 1997; Shaver et al. 1999; Furlanetto et al. 2006). Several current and next-generation experiments such as the Giant Metrewave Radio Telescope (GMRT, Paciga et al. 2013), the Low Frequency ARray (LOFAR, van Haarlem et al. 2013), the Murchison Widefield Array (MWA, Tingay et al. 2013; Bowman et al. 2013), the New Extension in Nançay Upgr.adding 6LoFAR (NENUFAR, Zarka et al. 2012; Mertens et al. 2021), the Owens Valley Radio Observatory – Long Wavelength Array (OVRO-LWA, Eastwood et al. 2019), Amsterdam-ASTRON Radio Transient Facility and Analysis Centre (AARTFAAC, Gehlot et al. 2020), the Hydrogen Epoch of Reionisation Array (HERA, DeBoer et al. 2017), the Square Kilometre Array (SKA, Koopmans et al. 2015), the Experiment to Detect the Global EoR Signature (EDGES, Bowman et al. 2018), the Shaped Antenna measurement of the background Radio Spectrum–3 (SARAS3, Nambissan 2021), the Large aperture Experiment to detect the Dark Ages (LEDA, Bernardi et al. 2016), and the Radio Experiment for the Analysis of Cosmic Hydrogen (REACH, de Lera Acedo 2019) are attempting to measure the fluctuations and global evolution of the 21-cm brightness temperature as a function of redshift.

However, the faint 21-cm signal from high redshifts is contaminated by astrophysical foreground emission that is 3–4 orders of magnitude brighter than the signal of interest. The astrophysical foregrounds consist of Galactic diffuse emission (synchrotron and free-free emission), and extra-galactic compact sources such as radio galaxies, supernova remnants, and other sources (Di Matteo et al. 2002; Zaldarriaga et al. 2004; Bernardi et al. 2009, 2010; Ghosh et al. 2012). Subtraction or
avoidance of these bright foregrounds poses a significant challenge in all 21-cm cosmology experiments. The interferometric experiments such as PAPER (Precision Array to Probe the Epoch of Reionisation) and HERA follow the so-called foreground-avoidance technique for separating the 21-cm signal from the foregrounds. This technique takes advantage of the fact that the spectrally smooth foregrounds occupy a small number of spectral modes and tend to reside within a ‘wedge-shaped’ region of the Fourier space, whereas the ‘EoR window’, in contrast to the ‘wedge’ region, should be dominated by a 21-cm signal and noise (Datta et al. 2010; Morales et al. 2012, 2019; Vedantham et al. 2012; Trott et al. 2012; Parsons et al. 2012; Hazleton et al. 2013; Dillon et al. 2014). On the other hand, 21-cm experiments with LOFAR, AARTFAAC, NENUFAR, and also the one planned with SKA follow the foreground-removal approach in their analysis strategy (Gehlot et al. 2019, 2020; Mertens et al. 2020). The 21-cm experiment with MWA utilises foreground subtraction in conjunction with foreground avoidance (Barry et al. 2019; Trott et al. 2020). Current foreground removal techniques used by experiments in the latter category include image deconvolution and source extraction algorithms such as CLEAN (Högberg 1974; Clark 1980; Cornell 2008; Offringa & Smirnov 2017), Duchamp (Whiting 2012), and PyBDSF (Mohan & Rafferty 2015) to model the extra-galactic compact sources as delta functions and Gaussians in image space. This is followed by subtraction of the model from the observed signal using direction-dependent (DD) calibration, for example with SAGECAL (Yatawatta 2016; Yatawatta et al. 2017). However, these traditional methods, largely developed for longer-baseline high brightness-temperature data, are sub-optimal for modelling large-scale diffuse emission, extended sources, and foreground emission below the confusion noise that dominates the observed signal. The latter is typically mitigated in these experiments using blind foreground removal techniques such as Wp smoothing (Harker et al. 2009), FastICA (Chapman et al. 2012), GMCA (Chapman et al. 2013), and GPR (Mertens et al. 2020) that exploit the spectral smoothness of the foregrounds to model and remove foregrounds from the observed data. Besides the intrinsic interest of studying properties of the diffuse Galactic emission, it is essential to include the diffuse (and compact) emission component in the instrumental gain calibration step regardless of the signal separation choices adopted by various experiments. Various investigations by Patil et al. (2016), Barry et al. (2016), Ewall-Wice et al. (2017), Mouri Sardarabadi & Koopmans (2019), and Byrne et al. (2019) have shown that using an incomplete sky model in the calibration step leads to significant suppression of the diffuse emission as well as the 21-cm signal of interest on shorter baselines that are dominated by diffuse emission. Since shorter baselines provide most of the sensitivity towards the 21-cm signal, it is crucial to calibrate these baselines accurately to prevent any signal suppression. One option to mitigate the effect of sky incompleteness is to remove the short baselines from calibration and include only longer baselines where the diffuse emission is resolved out (Patil et al. 2017). However, the exclusion of short baselines from calibration leads to a so-called excess variance on the excluded baselines in calibration (Patil et al. 2016; Barry et al. 2016; Ewall-Wice et al. 2017; Mouri Sardarabadi & Koopmans 2019), impacting the power spectrum estimation. Data from several 21-cm experiments such as MWA (Byrne et al. 2022), OVRO-LWA (Eastwood et al. 2018), and the LWA New Mexico station (Dowell et al. 2017) are already being used to develop diffuse sky maps to facilitate the precise calibration of 21-cm observations. As a part of the AARTFAAC Cosmic Explorer (ACE) project (Gehlot et al. 2020), the data from AARTFAAC-LBA are also being utilised to produce a wide-band map of the northern sky (∼10 arcmin resolution) at low frequencies with high fidelity due to its superb uv coverage.

In this work, we present the first ever wide-field images produced using the High-Band Antenna (HBA) observations of the LOFAR Amsterdam-ASTRON Radio Transients Facility And Analysis Centre (AARTFAAC) wide-field imager (Prasad et al. 2016) at 122 MHz. We explore multi-scale CLEAN and shapelet decomposition methods to model the diffuse emission in an extended region of around a 20° radius centred at the North Celestial Pole (NCP). Line et al. (2020) also present a similar study comparing multi-scale CLEAN and shapelet decomposition to model the bright extended source Fornax A using simulations and data from MWA. However, that study was focused on modelling sources with extended emission from a few arcmins up to a degree. In this pilot project, we focus on quantifying the spatial properties of the spectrally smooth diffuse emission in the field using the angular power spectrum technique. In the future, we plan to expand the current analysis by including spectral and polarisation information of the diffuse emission.

The paper is organised as follows: Sects. 2 and 3 briefly describe the observational set-up, preprocessing steps, calibration, and imaging scheme. The two diffuse foreground modelling methods and their comparison are presented in Sect. 4. Section 5 describes the angular power spectrum to quantify the properties of the diffuse emission. Finally, Sect. 6 provides a summary of the work and lays out the future steps and improvements.

2. Observations and preprocessing

We used the AARTFAAC-HBA wide-field imager to observe an extended region of an ∼20-degree radius around the NCP in the frequency range of 114–126 MHz, which is the primary observation window of the LOFAR-EoR Key Science Project (KSP; Patil et al. 2017; Mertens et al. 2020). The observational set-up and the preprocessing steps are discussed briefly in the following subsections.

2.1. The AARTFAAC wide-field imager

AARTFAAC is a LOFAR-based all-sky radio transient monitor (Kuijack et al. 2019). It piggybacks on ongoing LOFAR observations and taps the digital signal streams of individual antenna elements from six (A6 mode that uses ‘superterp’ stations) or twelve core stations (A12 mode that uses 12 central stations). The A6 mode consists of 288 dual-polarisation receivers – low band antenna (LBA) dipoles or HBA tiles – within a 300 m diameter circle, and the A12 mode consists of 576 such receivers spread across a 1.2 km diameter. The digitised signals from these receivers are tapped and transported to the AARTFAAC correlator prior to beam-forming. Due to current network capacity limitations, only 16 sub-bands can be correlated in the 16-bit mode. Each sub-band is 195.3 kHz wide and consists of up to 64 channels providing a maximum frequency resolution of 3 kHz, with an instantaneous system bandwidth of 3.1 MHz. The correlator subsystem, located at the Centre for Information Technology (CIT) at the University of Groningen (the Netherlands), is a GPU-based correlator that maximally handles 576 input signal streams per polarisation (1152 total streams) and produces XX, XY, YY, and YY correlations for all receiver pairs for every frequency channel with a 1-second integration. The output correlations can either be dumped as raw correlations on disks.
or routed to the AARTFAAC real-time calibration and imaging pipeline for transient detection (Prasad et al. 2016; Kuiack et al. 2019). Readers are referred to van Haarlem et al. (2013) and Prasad et al. (2016) for detailed information about the LOFAR and AARTFAAC system design and observing capabilities.

2.2. Observational set-up

We used the AARTFAAC-HBA system in A12 mode (A12-HBA hereafter) to observe the field around the NCP. For our observations, we targeted the 114–126 MHz frequency range corresponding to the redshift range of $z = 10.2–11.4$. Due to the currently limited bandwidth of 3.1 MHz, we adopted an observation strategy where we combined four different observations recorded within a span of a few weeks to cover the 12 MHz band. For each observation, sub-bands were sparsely spread in a frequency-comb configuration spanning the 12 MHz band. Sub-bands from each observation were interlaced and do not overlap. This observing strategy allows each observation to independently (and sparsely) span the 12 MHz bandwidth and continuous coverage of the 12 MHz band when combined together. Figure 1 shows a schematic of the sub-band set-up that we have adopted for the observations. Although higher time and frequency resolution is preferred for RFI flagging, we restricted the data resolution to lower values of 2 s and 195 kHz (to observe the NCP for a longer duration) due to the limited capacity of the AARTFAAC storage system. The raw correlation data were later transported to the LOFAR-EoR KSP processing system (dawn HPC cluster, Pandey et al. 2020), where all of the data processing and analysis were performed. The raw data were converted to a standard measurement set (MS) format using AARTFAAC2MS\(^1\) (Offringa et al. 2015) and the raw visibilities were phased to the NCP before preprocessing. The observational details of this data set are summarised in Table 1.

2.3. Data preprocessing

The preprocessing steps include RFI flagging and averaging the raw visibilities. We used AOFLAGGER (Offringa et al. 2010, 2012) to flag RFI-corrupted data. We also flagged all the visibilities corresponding to non-operational tiles in the data sets. The remaining data were averaged to a lower time resolution of 12 s. After averaging, the data volume of an 11-h observation of 3.1 MHz bandwidth was $\sim$1.7 TB. We noted that five out of six stations outside the superterp had significantly lower visibility amplitudes in all observations recorded during this first pilot programme. Furthermore, the visibilities corresponding to these stations showed extremely erratic behaviour even after calibration. Therefore, we also flagged the tiles corresponding to these five stations before the calibration step. Figure 2 shows the $\nu \tau$ coverage of the full A12-HBA array and after flagging the above stations. There is a significant reduction of long baselines due to the flagging of the five stations. We note that a single sub-band is sufficient for the purpose of the current analysis, that is to say to model and study the spatial properties of the spectrally smooth diffuse foreground emission, as the confusion noise level is reached in a single sub-band. The analysis of the full frequency range, including a power-spectrum analysis, will be presented in a future publication.

3. Calibration and imaging

Visibilities measured by a radio interferometer are corrupted by errors due to instrumental imperfections and environmental effects. These corruptions are broadly classified into two categories, namely direction-independent (DI) effects, such as complex receiver gains, global bandpass, and a global ionospheric phase, and DD effects, which change with the apparent direction of the incoming electromagnetic signals due to the antenna voltage patterns (and consequently the tile beam), ionospheric phase fluctuations, and Faraday rotation. Calibration refers to estimating the gains corresponding to these effects to obtain a reliable estimate of the true visibilities after the gain correction. We performed gain calibration in a self-calibration manner using the following steps:

1. The first step was to remove the bright sources, Cassiopeia A (Cas A) and Cygnus A (Cyg A) (with the apparent flux of several hundred Jansky), that superpose significant point spread function (PSF) side lobes over the field. We used the DD-calibration option within SAGECAL-co (Yatawatta 2015, 2016; Yatawatta et al. 2017) to subtract these sources from the raw visibilities. SAGECAL-co regularises the gain solutions with a spectrally smooth function in the gain calibration to improve the calibration quality. We used the Cas A and Cyg A shapelet model

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\(^1\) https://github.com/aroffringa/aartfaac2ms

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Table 1. Observational details of the data.

| Parameter                  | Value                        |
|----------------------------|------------------------------|
| Telescope                  | LOFAR-AARTFAAC               |
| Antenna configuration      | A12                          |
| Number of receivers        | 576 (HBA tiles)              |
| Number of pointings        | 1                            |
| Pointing centre (RA, Dec; J2000): | 0h0m0s, +90°00'00"    |
| Duration of observation    | 11 h                         |
| Observing frequency (and width) | 122 MHz (195.3 kHz)   |
| Primary Beam FWHM          | 28° at 122 MHz               |
| Field of View              | 625 deg\(^2\) at 122 MHz    |
| Polarisation               | Linear X–Y                   |
| Time, frequency resolution:| Raw Data 2 s, 195.3 kHz      |
|                           | After flagging 12 s, 195.3 kHz|
adopted from the LOFAR-EoR calibration sky model to subtract these sources using their inferred directional gains. We used a solution interval of 2 min and 5 ADMM (alternating direction method of multipliers) iterations with a regularisation factor of $\rho = 5$ (Yatawatta 2016). We excluded $|u| < 10$ (in units of wavelength) baselines from the calibration to avoid most of the large-scale diffuse emission biasing the calibration, but it is important to note that the diffuse emission extends over a much wider range of baselines as shown in later sections. At the current sensitivity level, we do not expect biases due to unmodelled diffuse emission on longer baselines overwhelming the calibration.

2. We performed DI calibration on the resulting visibilities after step 1. The initial calibration model consists of six sources listed in Table 2, with intrinsic flux values ($F_{\text{int}}$) taken from Cohen et al. (2007) for 3C220.3 and Baldwin et al. (1985) for the remaining sources. All sources, except for 3C61.1, are represented by delta functions and a power law representing their corresponding source spectra with an assumed yet typical spectral index of $\approx -0.8$. The radio galaxy 3C61.1 has a more complicated morphology, and its model was adapted from the intrinsic sky model used in the LOFAR-EoR calibration pipeline (Mertens et al. 2020). The 3C61.1 model uses delta functions and shapelets to represent the source, and a third-order log-polynomial represents the spectrum. We used a calibration solution interval of 2 min to maintain a significant signal-to-noise ratio per solution and carried out 5 ADMM iterations with a regularisation parameter of $\rho = 5$ using SAGECAL-CO (Yatawatta 2016). We also removed the $|u| < 10$ baselines during this step. We did not use a beam model during calibration, and the flux scale of the visibilities post-calibration is on an apparent flux scale (i.e. uncorrected for the average beam). Currently, the primary beam model for AARTFAAC-HBA tiles is not implemented in SAGECAL-CO, and efforts are ongoing to utilise the present LOFAR-HBA tile beam model for AARTFAAC-HBA calibration. Therefore, to avoid notable differential primary beam effects, all six sources chosen for this intermediate gain calibration step reside within a ~7$^\circ$ radius around the NCP. The corrected visibilities are close to the correct flux scale since the primary beam does not substantially change within this radius.

3. The calibrated visibilities were imaged and deconvolved using the multi-scale CLEAN feature of WS/CLEAN (Offringa et al. 2014; Offringa & Smirnov 2017), using a cleaning threshold of 0.7$\sigma$, with a ‘Briggs –0.1’ weighting-scheme and $|u| > 50$ baselines in order to avoid bright degree-scale diffuse emission severely affecting the deconvolution process.

4. The steps 2 and 3 were repeated three times in a ‘selfcal’ loop using the improved calibration model (updated with the clean components) obtained after each iteration. For each iteration, we used an auto-masking threshold (Offringa & Smirnov 2017) of 8$\sigma$, 5$\sigma$, and 3$\sigma$, respectively, where $\sigma$ is the image rms. The final CLEAN model contains 4924 components (delta functions and Gaussians) to represent the compact sources in the field.

Table 2. List of sources in the initial calibration model.

| Source      | Intrinsic Flux ($F_{\text{int}}$) | References                  |
|-------------|----------------------------------|-----------------------------|
| 3C61.1      | 38 Jy (151.5 MHz)                | Baldwin et al. (1985)       |
| 3C220.3     | 38 Jy (150 MHz)                  | Cohen et al. (2007)         |
| LQAC 244+085 001 | 6.2 Jy (151.5 MHz)    | Baldwin et al. (1985)       |
| NVSS J011045+873822 | 5.1 Jy (151.5 MHz)   | Baldwin et al. (1985)       |
| NVSS J190350+853648 | 4.9 Jy (151.5 MHz)   | Baldwin et al. (1985)       |
| NVSS J062205+871948 | 4.9 Jy (151.5 MHz)   | Baldwin et al. (1985)       |

Fig. 2. Single sub-band (122 MHz) $uv$ coverage of the A12-HBA array towards the NCP for 11 h of synthesis. Left panel: $uv$ coverage of the full A12-HBA array. Right panel: same as on the left, but with flags included. The colour scale corresponds to the number of baselines in $uv$ cells of size $(u, v) = (1,1)$ (in units of wavelength). The dotted black circle shows $|u| = 120$, which is used as the baseline range to model the diffuse structure in later sections. The effect of flagging five stations is clearly visible in the $uv$ coverage shown in the right panel.
Fig. 3. Left panel: Stokes I dirty image of a ~20 degree radius field around the NCP using a single sub-band (122 MHz) of A12-HBA data and all A12-HBA baselines (|u| < 400) available after flagging. Right panel: Stokes I image for the same field with the same imaging parameters and baseline range, but using LOFAR-HBA station beam-formed data that lack the shortest baselines. The dotted circles and spokes represent different declinations and right ascension, respectively.

5. We finally imaged the DI-calibrated visibilities obtained after step 4 with WSclean using a ‘Briggs +0.5’ weighting scheme in all subsequent analyses.

Figure 3 shows single sub-band Stokes I dirty images of the NCP field produced using A12-HBA and LOFAR-HBA data at 122.06 MHz (195.3 kHz bandwidth). The A12-HBA system has an ~25 times larger field of view compared to the LOFAR-HBA system. Galactic large-scale diffuse emission is clearly visible around NCP in the A12-HBA image (see also Bernardi et al. 2010). Although the diffuse emission is also partly present in LOFAR-HBA, it is not visible because LOFAR-HBA has a much lower short-baseline density and a total absence of baselines shorter than 40 metres (|u| < 15 or ℓ < 100 at 122 MHz) compared to A12-HBA.

4. Modelling the diffuse galactic emission

In this section, we present two approaches to model the diffuse structure around the NCP as seen in Fig. 3. In the first approach, we used multi-scale CLEAN deconvolution with WSclean (Offringa & Smirnov 2017) to model the diffuse structure. In the second method, we used an orthonormal set of Hermite polynomial basis functions called ‘shapelets’ (Refregier 2003; Yatawatta 2011) to model the diffuse structure.

4.1. Removal of compact sources

Before proceeding with the diffuse foreground modelling, the bright compact sources needed to be removed from the map. We used the CLEAN component model obtained during the gain calibration (see step 4 in Sect. 3) to subtract 4924 components from the data. Figure 4 shows the Stokes I image of the NCP field before and after the subtraction of the CLEAN model. The images were produced using the Briggs −0.1 weighting scheme with u > 50 baselines. We observe that subtracting the CLEAN model removes most of the compact sources, leaving only faint residuals of the order of a few hundred mJy rms. The images do not visually reveal signatures of diffuse emission because of the baseline cut used during the imaging process. We also see that the subtraction of some of the brightest sources leaves negative or ring-like artefacts near their source location. Factors such as imperfect calibration and imperfect source modelling are the likely cause. These artefacts can be further mitigated by using DD calibration to subtract the bright sources. We plan to employ DD calibration for the subtraction of bright sources using several directions in future analyses. For the purpose of this work, that is to say analysing the properties of the diffuse foregrounds, these minor artefacts are not important.

We derived an estimate of the confusion noise for AART-FAAC from the classical confusion limit ($\sigma_c$) using the relation from van Haarlem et al. (2013):

$$\sigma_c = 30 \left( \frac{\theta}{1''} \right)^{1.54} \left( \frac{\nu}{74 \text{ MHz}} \right)^{-0.7} \text{[\mu Jy beam}^{-1}],$$

where $\theta$ is the angular resolution (FWHM) and $\nu$ is the observation frequency. A12-HBA has an angular resolution of ~7′ at 122 MHz, yielding a confusion limit of $\sigma_c \sim 230 \text{ mJy beam}^{-1}$. The standard deviation of the residuals, after cleaning, for the inner 10° region of the field is ~220 mJy. These two values are consistent with each other, assuming that the primary beam correction is small for this inner 10° region. In the future, we plan a deeper multi-frequency CLEAN step by combining sub-bands spanning a wide frequency range along with an improved direction-dependent calibration step that includes an HBA-tile beam model. Figure 5 shows the Stokes I image of the residual visibilities after subtraction of the 4924 component CLEAN model, produced using $u \leq 120$ baselines. The corresponding A12-HBA PSF (shown in Fig. 6) is well-behaved with few percent side-lobe levels within an ~3° radius and close to zero...
Fig. 4. Left panel: Stokes I CLEAN restored image of the NCP at 122 MHz after CLEAN deconvolution, produced using a ‘Briggs −0.1’ weighting scheme and with $u > 50$ baselines. Right panel: Stokes I CLEAN residual image after subtraction of the CLEAN model with 4924 components from the data. The residuals are consistent with the confusion noise.

Fig. 5. Stokes I dirty image of the residual visibilities after the subtraction of 4924 CLEAN model components. The image was produced using a ‘Briggs +0.5’ weighting scheme (which gives more weight to short baselines to better visualise the diffuse emission), $u \leq 120$ baseline range, and a Gaussian taper of 30'.

elsewhere. We thus modelled this residual diffuse emission using the two methods mentioned above.

4.2. Modelling with multi-scale CLEAN

We used the multi-scale deconvolution algorithm implemented in WS克莱恩 (Offringa & Smirnov 2017) to model the diffuse structure observed in Fig. 5. We performed deconvolution with the following settings: a Briggs +0.5 weighting scheme, an auto-mask of $3\sigma$, a major iteration cleaning gain (mgain) of 0.8, and a clean stopping threshold of $0.6\sigma$. The Briggs weighting scheme with a threshold greater than zero gives more weight to short baselines and reveals diffuse emission better. Figure 7 (top row) shows the Stokes I image of the field before and after subtracting the diffuse foreground model obtained from multi-scale CLEAN. We observe that multi-scale CLEAN is able to model the extended emission at different scales using Gaussians and point sources, adequately capturing the diffuse flux. The algorithm also models the compact residuals (both positive and negative) initially missed by the compact model subtraction step.

After the subtraction of the diffuse model, the residual appears to be devoid of a diffuse structure, with a standard deviation of $\sim 500$ mJy inside the inner region of the image. We note that the CLEAN algorithm is sensitive to image weighting and the
Fig. 7. **Top row:** Stokes $I$ dirty image before subtraction of the diffuse structure (left panel), the diffuse model obtained with multi-scale CLEAN (middle panel), and the residual Stokes $I$ image after subtraction of the CLEAN model (right panel). **Bottom row:** same as the top row, but with the shapelet decomposition technique to model the diffuse structure. These images were produced using Briggs $+0.5$ and $u \leq 120$ baselines with a Gaussian taper of $30'$.

4.3. Modelling with shapelets

Yatawatta (2011) showed that the use of orthonormal basis functions, for example Cartesian shapelets (Refregier 2003) or prolate spheroidal wave functions (PWSF; Slepian & Pollak 1961; Landau & Pollak 1961) in radio interferometric image deconvolution, provides improved image fidelity and a larger dynamic range. In the image domain, $(l,m)$, shapelet basis functions can be written as follows (Yatawatta 2011):

$$\phi_{n_1,n_2}(l,m,\beta) = \frac{1}{2^{n_1+n_2} \pi \beta^{n_1+n_2}} H_{n_1}(l/\beta) H_{n_2}(m/\beta) \times \exp \left[ -\frac{(l^2 + m^2)}{2\beta^2} \right],$$

(2)

where the functions $H_{n_1}$ and $H_{n_2}$ are the Hermite polynomials of order $n_1$ and $n_2$, which are integer values, and the value of $\beta$ is the model scale factor. We demonstrate the use of Cartesian shapelets to model the diffuse structure observed in A12-HBA data using the SHAPELET_GUI$^3$ tool. We used $25 \times 25$ basis functions for the shapelet decomposition using L1-norm regularisation. We optimised the model scale during the process. Figure 7 (bottom row) presents the Stokes $I$ images before and after shapelet model subtraction, as well as the shapelet model of the diffuse structure obtained from the decomposition. We note that the shapelet model captures the large-scale diffuse structure within the primary beam. The residuals within the primary beam have a standard deviation of $\sim 540$ mJy, which is approximately the same as residuals after CLEAN diffuse model subtraction. These residuals are most likely the unmodelled compact sources and sources below the confusion noise. However, the diffuse structure outside the primary beam is rather poorly modelled. This is mainly due to the finite support of the basis functions and using a single shapelet model with a large number of basis functions leading to a sub-optimised scale factor ($\beta$, width of the basis functions). This results in an inadequate performance of the shapelet model in capturing the structure outside the primary beam. The performance of the shapelet decomposition modelling is expected to be enhanced by optimising the number of basis functions used for the decomposition and their scale factor ($\beta$). Additionally, using multiple shapelet models to capture the diffuse structure in different regions in the image space and using primary-beam corrected images is expected to improve the shapelet model.

$^3$ Developed by Sarod Yatawatta. [https://github.com/SarodYatawatta/shapeletGUI](https://github.com/SarodYatawatta/shapeletGUI)
4.4. Comparing the two diffuse emission modelling approaches

From the visual inspection of the two models in Fig. 7, we find that, in this particular set-up, the multi-scale CLEAN deconvolution method captures compact sources and diffuse structures at a range of angular scales. On the other hand, the shapelet decomposition captures the structure on large scales significantly better. However, it is less effective – without hugely increasing the number of basis functions and shapelets – in modelling compact sources, which is apparent from the lack of a compact structure in the shapelet model in Fig. 7. We infer that in the current implementation, both multi-scale CLEAN and shapelet decomposition are able to model the large-scale (order of several degrees) diffuse Galactic emission. However, the shapelet model performs poorly outside the primary beam and is inefficient at capturing the structure on small scales (<1 degree). A possible improvement in the CLEAN model may be achieved by tweaking the image weighting scheme and the scales used in deconvolution. Similarly, optimising the number of basis functions, their scale factor, and using multiple shapelets are expected to enhance the shapelet model. However, CLEAN deconvolution provides the added benefit of fitting a spectrum to capture the spectral behaviour of the diffuse structure, which is currently not the case with shapelet decomposition. The inclusion of spectral indices (per basis function) in the shapelet model is currently under development. For future analyses, we plan to improve the analysis and modelling process by adding more data over a wide range of frequencies and by modifying various parameters described above. We also plan to explore a hybrid approach to build the sky model by combining the two methods, where the CLEAN model is used to capture small-scale structures and compact sources, and shapelets are used to represent the large-scale diffuse structures. The more complete diffuse emission model will consist of information on a wide range of spatial scales and spectral information. This model can also be utilised to improve the calibration and foreground removal (using DD calibration) of the LOFAR-EoR and AARTFAAC-HBA observations.

5. The angular power spectrum

The angular power spectrum is a commonly used metric to study the spatial properties of the foreground emission. We use the angular power spectrum, \( C_\ell \), to describe the observed diffuse emission in the NCP field. The angular power spectrum \( C_\ell \) is defined as follows (see e.g., Seljak 1997; Bernardi et al. 2009):

\[
C_\ell = \frac{1}{N_\ell} \sum_I \tilde{I}(\ell) \tilde{I}^*(\ell),
\]

where \( \tilde{I}(\ell) \) is the spatial Fourier transform of an image \( I \) (in units of Kelvins), \( \ell = 2\pi \alpha \) is a two-dimensional vector and Fourier dual to the angular coordinate vector in image space, \( N_\ell \) is the number of samples in a given azimuthal bin (annulus) of width \( \delta \ell = 8.0 \), and the scalar multipole moment \( \ell \) is the average of \( |I| \) in a given azimuthal bin. The multipole moment \( \ell \) is related to the angular scale \( \Theta \) (half-width half maximum) in degrees as \( \ell = \Theta / 90^\circ \). We used the Stokes I images to estimate \( C_\ell \). The images were Fourier transformed along the spatial axes using fast Fourier transform (FFT). Because the shapelet modelling performs poorly outside the primary beam, we multiplied the images with a spatial Tukey (tapered cosine) window before the FFT to suppress the emission outside the 15° radius. We normalised the Fourier transform of the images with the PSF to remove the effect of the weighting scheme applied during imaging. It is important to note that we did not apply a primary-beam correction during the estimation of \( C_\ell \), nor did we correct for the curvature of the sky. We expect the A12-HBA primary beam (or the LOFAR-HBA tile beam) to be fairly regular on the sky region within the primary beam FWHM. Any beam taper is absorbed in the model and should not affect the single sub-band analysis. The sky-curvature manifests itself as the \( w \) term in interferometric imaging. The A12 array is highly co-planar, with the maximum \( w \) term only being \( -1-2\% \) (~6 in units of wavelength) of the longest baseline. Additionally, the \( w \)-stacking algorithm of WCSKLEAN in the current analysis uses 48 \( w \) layers to correct for the wide-field-related and sky-curvature-related effects. We, therefore, expect that both of these effects are limited and of second order in the current analysis.

Figure 8 presents the angular power spectrum \( \Delta_\ell^2 \) of the A12-HBA Stokes I image before and after subtraction of the 4924 component CLEAN model. The solid orange, blue, and grey curves correspond to the emission in the field (data before point source CLEAN model subtraction), the point source CLEAN model, and the residual emission, respectively. The dashed blue and grey curves represent the best-fit profiles of the point source CLEAN model \( \Delta_\ell^{\text{CLEAN}}(\ell) \) and the residual emission \( \Delta_\ell^{\text{residual}}(\ell) \), respectively. The error bars on data correspond to the 2\( \sigma \) uncertainty due to sample variance.

\[
\Delta_\ell^{\text{CLEAN}} = A \left( \frac{\ell}{\ell_0} \right) \alpha,
\]

where \( A \) and \( \alpha \) are the scale factors for the wide-field-related and sky-curvature-related effects, respectively. We, therefore, expect that both of these effects are limited and of second order in the current analysis.

![Fig. 8. Comparison of the angular power spectrum (\( \Delta_\ell^2 \)) of the A12-HBA Stokes I image before and after subtraction of the 4924 component CLEAN model. The solid orange, blue, and grey curves correspond to the emission in the field (data before point source CLEAN model subtraction), the point source CLEAN model, and the residual emission, respectively. The dashed blue and grey curves represent the best-fit profiles of the point source CLEAN model (\( \Delta_\ell^{\text{CLEAN}}(\ell) \)) and the residual emission (\( \Delta_\ell^{\text{residual}}(\ell) \)), respectively. The error bars on data correspond to the 2\( \sigma \) uncertainty due to sample variance.](attachment:image.png)
where $A$ and $\alpha$ as well as $A'$, $B'$, and $\alpha'$ are the free parameters for the CLEAN model fit and the residual emission fit, respectively. We chose $\ell_0 = 180$ which corresponds to an angular scale of $\Theta = 1\degree$. The best-fit parameter values for the two models are listed in Table 3. The data and the point source CLEAN model has a power-law-like behaviour on $\ell \gtrsim 60$. Fitting the angular power spectrum of the point source CLEAN model with Eq. (4) yields a best-fit power-law index $\alpha = 1.99 \pm 0.09$, which is consistent with the angular power spectrum of unresolved and unclustered sources, that is $\Delta_0^2 \propto \ell^2$ (Tegmark & Efstathiou 1996). This suggests that the compact sources begin dominating the power on baselines of $u \gtrsim 10$ or angular scales of $\Theta \lesssim 3\degree$ ($\ell \gtrsim 60$). The angular power spectrum $\Delta_{\ell}^2$ of the residual emission is flat within $20 \leq \ell \leq 200$, suggesting that $C_\ell \propto \ell^{-2}$. This is consistent with the angular power spectrum of the Galactic diffuse emission, $C_\ell \propto \ell^{-2.6}$, observed by Bernardi et al. (2009).

However, the power on $\ell > 200$ is possibly dominated by thermal noise and low-level emission below confusion noise, and it starts to exhibit a power-law-like behaviour. As revealed from the fit, the residual diffuse emission has a brightness temperature variance of $\Delta_{\ell=180}^2 = (145.64 \pm 13.61) \text{K}^2$ at 122 MHz on angular scales of 1 degree, and it is consistent with $C_\ell \propto \ell^{-2.0}$ in the $20 \leq \ell \leq 200$ range. Using observations of the NCP with the Westerbork Synthesis Radio Telescope (WSRT), Bernardi et al. (2010) reported $\Delta_{\ell=120}^2 \sim 14 \text{K}^2$ at 150 MHz, which corresponds to $\Delta_{\ell=120}^2 \sim 40 \text{K}^2$ at 122 MHz when extrapolated with the spectral index of $-2.6$. Additionally, Offringa et al. (2022) observed $\Delta_{\ell=120}^2 \sim 3 \text{K}^2$ for the field centred at the ‘coldest patch’ of the northern Galactic hemisphere (Kogut et al., 2011), and $\Delta_{\ell=120}^2 \sim 10 \text{K}^2$ for another field $\sim 10\degree$ away from the coldest patch at 140 MHz with LOFAR. Whereas, we observe $\Delta_{\ell=120}^2 \sim 130 \text{K}^2$ in our analysis, that is to say around four times the power observed by Bernardi et al. (2010). We hypothesise that the high power observed in our analysis is possibly due to the limited power in the AARTFAAC data (195 kHz) used in this study compared to the analyses in Bernardi et al. (2010) (40 MHz) and Offringa et al. (2022) (48 MHz). Moreover, we did not apply any noise correction (instrumental or confusion) contrary to Bernardi et al. (2010). We defer the latter to the future analyses.

5.1. Power spectra from diffuse foreground modelling methods

The angular power spectrum is also a useful metric to compare the two foreground modelling methods, in other words multi-scale CLEAN and shapelet decomposition, that we demonstrated in Sect. 4. We used the images shown in Fig. 7 for the two methods to determine the corresponding angular power spectra $\Delta_\ell^2$. We used the same methodology as mentioned in the previous section to determine $C_\ell$. Figure 9 shows the angular power spectra $\Delta_\ell^2$ of the residuals after subtraction of CLEAN and shapelet diffuse models obtained from the two methods.

We observe that the multi-scale CLEAN method leads to lower residuals than the shapelet model on $\ell < 70$ modes ($\Theta \lesssim 2.3\degree$). However, the shapelet model produces slightly lower residuals on $70 \leq \ell < 200$ compared to multi-scale CLEAN. The residuals on $\ell > 200$ behave similarly to the data, probably due to the noise in the data. It is important to note that the two methods – and the residuals obtained from these – compared in this analysis use a very specific set-up. A detailed investigation to study and quantify finer differences between the two methods will be performed in future analyses.

6. Summary and future work

In this work, we have presented the first ever wide-field images obtained with the LOFAR AARTFAAC-HBA system in A12 mode. In particular, we find strong degree-scale diffuse Galactic Stokes $I$ radio emission at 122 MHz within a $\sim 20$-degree radius field around the NCP, which is one of the primary windows of the LOFAR EoR project (Yatawatta et al. 2013; Mertens et al. 2020). We have compared two different methods for modelling this diffuse emission, namely multi-scale CLEAN deconvolution and shapelet decomposition. We used angular power spectrum to quantify the behaviour of different foreground components, notably point sources and diffuse emission. The main results of this work are summarised as follows:

- Stokes $I$ radio emission, as seen by the LOFAR AARTFAAC-HBA system around the NCP at 122 MHz on baselines shorter than 120 wavelengths, is dominated by large-scale diffuse emission. The angular power spectrum of the emission in the field is dominated by the point sources on scales smaller than 3 degrees ($\ell \gtrsim 60$). After subtraction

| Parameter                  | Best-fit value   |
|----------------------------|------------------|
| $A$                        | $1438.75 \pm 111.08$ |
| $\alpha$                   | $1.99 \pm 0.09$   |
| Residual emission model    |                  |
| $A'$                       | $128.16 \pm 13.45$ |
| $B'$                       | $17.48 \pm 2.08$  |
| $\alpha'$                  | $3.00 \pm 0.47$   |

Table 3. Best-fit parameters.
of the point source CLEAN model, the residuals are dominated by the diffuse emission scales larger than a degree ($\ell \lesssim 200$). This diffuse emission, with $10^3$ times more power than the 21-cm signal, can have a considerable impact on the calibration of any radio-interferometric instrument (e.g., LOFAR, MWA, HERA, NUNUFR, LWA, and SKA) if this emission is not part of the sky model during instrumental gain calibration (or filtered out before calibration) or if their baselines are not excluded during calibration.

- We show that, with our particular set-up, multi-scale CLEAN can model the small and intermediate scales well, but it shows a slightly worse performance on intermediate scales than the shapelet decomposition, which captures the large-scale diffuse emission well. However, it is incapable of modelling the emission on scales smaller than several degrees.

- The diffuse emission has a brightness temperature variance of $\Delta T_B = 145.64 \pm 13.61 \, K^2$ at 122 MHz on angular scale of 1 degree, and it is consistent with $C_\ell \propto \ell^{-2.6}$ in the $20 \lesssim \ell \lesssim 200$ range.

This analysis in this pilot work is admittedly based only on data from a single sub-band at 122 MHz. Despite this restriction, for the first time using AARTFAAC-HBA as a wide-field imaging instrument, we have convincingly shown that large-scale diffuse emission dominates the emission in Stokes $I$ on degree scales and larger. This was previously much harder to assess due to the limited short-baseline coverage of LOFAR in beam-formed mode. In the current analysis, we used traditional CLEAN deconvolution to model and subtract the compact sources before modelling the diffuse structure. We suspect that artefacts left over from the deconvolution and subtraction of compact sources may lead to low-level systematics in the diffuse emission models. In future analyses, we plan to implement DD calibration to subtract the compact sources instead of just using CLEAN deconvolution. It is expected to mitigate the systematics arising from poorly subtracted compact sources while taking the primary beam and ionospheric effects into account. In addition to this, we plan to include the following improvements in future analyses for accurate modelling of the diffuse emission:

- Including an HBA-tile beam model in the gain calibration, which allows us to (i) set an absolute flux scale, (ii) improve the calibration quality, (iii) perform deeper deconvolution during imaging, and (iv) improve the modelling of compact sources and diffuse emission.

- Expand on this analysis to a broader frequency range to obtain a complete spatial and spectral model of the diffuse emission.

- Explore a hybrid approach to model the emission on a wide range of spatial scales by combining multi-scale CLEAN to model small-scale compact emission and shapelet decomposition to model large-scale diffuse emission.

- Extend the analysis to model diffuse polarised emission in Stokes $Q$ and $U$. Wide-field polarisation studies will enable us to understand the behaviour and morphology of polarised foregrounds on very large scales and how it instrumentally leaks to Stokes $I$ (Asad et al. 2015, 2016, 2018; Nunhookee et al. 2017; Byrne et al. 2022).

We expect that the diffuse foreground model obtained after including the above-described improvements in the analysis should be sufficient in removing the diffuse emission around the NCP on angular scales and frequencies used to obtain the model regardless of the instrument design. The diffuse emission model will be included in the sky model used in the LOFAR-EoR and NUNUFR-CD calibration pipelines. The improved diffuse model will also be made available for public use in the form of a git repository. The CLEAN and shapelet models obtained in the current analysis may be obtained by submitting a request to the corresponding author.

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