We present a galaxy group catalog spanning the redshift range \(0.1 \lesssim z \lesssim 1\) in the \(\sim 10^2\) COSMOS field, based on the \(\sim 10,000\) zCOSMOS spectra. The performance of both the Friends-of-Friends (FOF) and Voronoi–Delaunay method (VDM) approaches to group identification has been extensively explored and compared using realistic mock catalogs. We find that the performance improves substantially if groups are found by progressively optimizing the group-finding parameters for successively smaller groups, and that the highest fidelity catalog, in terms of completeness and purity, is obtained by combining the independently created FOF and VDM catalogs. The final completeness and purity of this catalog, both in terms of the groups and of individual members, compares favorably with recent results in the literature. The current group catalog contains 102 groups with \(N \geq 5\) spectroscopically confirmed members, with a further \(\sim 700\) groups with \(2 \leq N \leq 4\). Most of the groups can be assigned a velocity dispersion and a dark-matter mass derived from the mock catalogs, with quantifiable uncertainties. The fraction of zCOSMOS galaxies in groups is about 25% at low redshift and decreases toward \(\sim 15\%\) at \(z \sim 0.8\). The zCOSMOS group catalog is broadly consistent with that expected from the semianalytic evolution model underlying the mock catalogs. Not least, we show that the number density of groups with a given intrinsic richness increases from redshift \(z \sim 0.8\) to the present, consistent with the hierarchical growth of structure.

**Key words:** catalogs – galaxies: clusters: general – galaxies: high-redshift – methods: data analysis

**Online-only material:** machine-readable tables

1. INTRODUCTION

Groups and clusters of galaxies are the most massive virialized structures in the universe. They are important for several reasons. First, groups and clusters define the environment in which most galaxies actually reside and in which we may expect many important processes determining the evolution of galaxies (e.g., Voit 2005). Studying the properties of galaxies in groups at different redshifts is a direct probe of how the local environment affects the formation and evolution of galaxies with cosmic time. Second, characterization of galaxies in groups provides information about the galactic content of dark matter (DM) halos. This yields statistical quantities such as the halo occupation distribution (e.g., Collister & Lahav 2005) or the conditional luminosity function (e.g., Yang et al. 2008) which themselves yield useful constraints on various physical processes that govern the formation and evolution of galaxies. Finally, the number density and clustering of groups strongly depend on cosmological parameters and thus are a potentially sensitive probe of the underlying cosmological model (e.g., Bahcall et al. 2003; Gladders et al. 2007; Rozo et al. 2009).
From an observational point of view, there are many ways to identify a group. In the current lambda cold dark matter (ΛCDM) framework, it is natural to associate groups with DM halos, and this is the definition adopted by most authors. Therefore, throughout this paper we refer to a “group” as a set of galaxies occupying the same DM halo.

There are many different observational techniques to identify groups in the local and distant universe in use today. Groups can be detected in the optical/near-infrared (NIR; e.g., Gal 2006), by diffuse X-ray emission (e.g., Pierre et al. 2006; Finoguenov et al. 2007), by the Sunyaev–Zel’dovich effect in the cosmic microwave background (e.g., Carlstrom et al. 2002; Voit 2005), by particular wide-angle tailed (WAT) galaxies (e.g., Blanton et al. 2003), and through cosmic shear due to weak gravitational lensing (e.g., Feroz et al. 2008). Each of these methods has its own advantages and problems (see, e.g., Voit 2005; Johnston et al. 2007, Section 1), and the choice of a particular method might depend on the desired application.

If one aims to study the galaxy population in groups, searching for groups directly in large optical galaxy surveys is relatively straightforward and efficient. There are many different methods discussed in the literature to identify groups in an optical survey (for a review see, e.g., Gerke et al. 2005, Section 4.1; Gal 2006).

In essence, these aim to identify overdensities in redshift space, luminosity, and/or color space, depending on the availability of redshift information and/or photometry. Whatever method is used, it should conform to the following general rules (see, e.g., Gal 2006): first, it should be based on an objective, automated algorithm to minimize human biases. Second, the algorithm should impose minimal constraints on the physical properties of the clusters to avoid selection biases. The latter point is especially important if one aims to investigate the evolution of the galaxy population in groups. For instance, it has been shown that the addition of color information provides a powerful tool to find clusters in the universe. There are methods such as the Cluster Red Sequence (CRS) method (Gladders & Yee 2000) or the maxBCG algorithm (Hansen et al. 2005; Koester et al. 2007a) which are based on the fact that the most luminous galaxies in clusters inhabit a tight sequence in the color–magnitude diagram called the “red sequence.” Using the red-sequence information, these methods have proved to be very successful in finding clusters in the local (Koester et al. 2007b) and the distant universe up to redshift $z \sim 1$ (Gladders & Yee 2005). A further advantage of these methods is that no redshift information is needed. However, clearly the requirement of a substantial population of red-sequence galaxies inhabiting the red sequence may impose a preselection that makes evolutionary studies more difficult.

The large number of accurate spectroscopic redshifts available for the large numbers of galaxies from the zCOSMOS redshift survey in the COSMOS field (Scoville et al. 2007) enables us to use the most fundamental signature of groups—overdensities in redshift space—without recourse to additional color information. Nevertheless, even with precise spectroscopic redshifts, to identify groups in redshift space one has to deal with certain difficulties: first, the peculiar velocities of galaxies in groups elongate groups in the redshift dimension (the “fingers-of-God” effect). This effectively decreases the galaxy density within groups in redshift space, and thus makes them harder to detect, and may cause group members to intermingle with other nearby field galaxies or even to merge into another nearby group. It is almost impossible to separate interlopers from real group galaxies if they appear within the group in redshift space. Second, in magnitude-limited surveys such as zCOSMOS, the mean density of galaxies decreases with redshift. So any algorithm based on the distance between neighboring galaxies has to take into account the dependence of the mean galaxy separation with redshift. Third, the observational selection of galaxies (e.g., inhomogeneous sampling rate in the spectroscopic survey) frequently produces additional complications.

To cope with these difficulties, some forms of the traditional Friends-of-Friends (FOF) algorithm (Huchra & Geller 1982) are still widely used (e.g., Eke et al. 2004; Berlind et al. 2006), although FOF has some well known shortcomings (e.g., Nolthenius & White 1987; Frederic 1995). For instance, the FOF algorithm depends sensitively on the value of the linking length, and can merge neighboring groups into single big groups, or fragment large groups into smaller pieces.

Until now, there have not been many spectroscopic redshift surveys searching for groups at high redshift. Carlberg et al. (2001) describe a group catalog obtained from CNOC2 in the redshift range $0.1 \lesssim z \lesssim 0.5$. For the redshift range $z \gtrsim 0.5$ only the DEEP2 redshift survey (Davis et al. 2003), covering a total area of $\sim 3$ deg$^2$ and redshift range of $0.7 \lesssim z \lesssim 1.4$, has sufficient size and sampling rate to identify a large number of groups in redshift space. To achieve this, Gerke et al. (2005, 2007) have adapted the Voronoi–Delaunay method (VDM) of Marinoni et al. (2002), which has claimed to compensate for some of the shortcomings of the traditional FOF algorithm.

The aim of this paper is to create a group catalog from the $\sim 10,000$ spectra in the zCOSMOS 10 k sample (S. J. Lilly et al. 2009, in preparation) to enable the study of the group population over the redshift range $0.1 \lesssim z \lesssim 1$. We will compare the performance of both the FOF and VDM algorithms on the 10 k sample, and try to optimize the group-finding methods by the introduction of a “multirun procedure.” In Section 2, we describe the 10 k sample and the corresponding realistic mock catalogs that were generated to test the group-finding algorithms.

Section 3 gives a detailed description of our adopted group-finding method, and discusses the performance of the two groupfinders. In Section 4, we present the 10 k group catalog, and describe how basic group properties are estimated.

Section 5 compares the 10 k group catalog to the mocks and to 2dFGRS. Finally, Section 6 summarizes the paper. Where necessary, a concordance cosmology with $H_0 = 73$ km s$^{-1}$ Mpc$^{-1}$, $\Omega_m = 0.25$, and $\Omega_{\Lambda} = 0.75$ is adopted. All magnitudes are quoted in the AB system.

2. DATA

2.1. zCOSMOS Survey

zCOSMOS is a spectroscopic redshift survey (Lilly et al. 2007; S. J. Lilly 2009, in preparation) covering the $\sim 1.7$ deg$^2$ COSMOS field (Scoville et al. 2007). The redshifts are measured with the VLT using the VIMOS spectrograph.
(Le Fèvre et al. 2003). The zCOSMOS survey is split into two parts. The first part, “zCOSMOS-bright,” is a pure magnitude-selected survey with $15 \leq I_{AB} \leq 22.5$, $I_{AB}$ the F814W Hubble Space Telescope (HST)/ACS band (Koekemoer et al. 2007). This magnitude limit will yield a survey of approximately 20,000 galaxies in the redshift range $0.1 \lesssim z \lesssim 1.2$. Repeated observations of some zCOSMOS galaxies have shown that the redshift error is approximately Gaussian distributed with a standard deviation of $\sigma_z = 100$ km s$^{-1}$. The second part of zCOSMOS, “zCOSMOS-deep,” aims at observing about 10,000 galaxies in the redshift range $1.5 \lesssim z \lesssim 3.0$ selected through a well-defined color criteria.

To date, about a half of zCOSMOS-bright has been completed yielding about 10,500 spectra (S. J. Lilly et al. 2009, in preparation). Among these redshifts about 15% are classified as unreliable. For the group catalog, we have accepted all objects with the confidence classes 4 and 3, 9.5, 9.3, 2.5, 9.4, 2.4, 1.5, and 1.4 (see S. J. Lilly et al. 2009, in preparation). The redshifts with these confidence classes constitute 86% of the whole 10 k sample and have a spectroscopic confirmation rate of 98.6% as found by duplicate observations. After removing the stars (~5%), we finally end up with a sample of 8417 galaxies with usable redshifts (“10 k sample”).

At the current stage of the survey, the spatial spectroscopic sampling rate of galaxies across the COSMOS field is very inhomogeneous, and there are clearly some linear features such as stripes visible (see Figure 5 of S. J. Lilly et al. 2009, in preparation). Since this will affect the number of detectable groups in this sample in a nontrivial way, we have created mock catalogs that have the same kind of inhomogeneous coverage. To create the group catalog and generate the statistics describing the fidelity of the catalog, the groupfinders were applied to the whole field spanning the range $149:47 \leq \alpha \leq 150:77$ and $1:62 \leq \delta \leq 2:83$. However, for some applications discussed below we restrict ourselves to the “central region” of the COSMOS field defined by $\alpha = 150^\circ \pm 0:4$ and $\delta = 2:15 \pm 0:4$, since this region is relatively complete compared to the total field. Only about 25% of the area has a completeness lower than 30% while for the whole field this area constitutes more than 50%.

The number of galaxies per unit redshift $dN_{gal}/dz$ is shown in Figure 1. There are two striking density peaks at redshifts $z \sim 0.3$ and ~0.7.

### 2.2. zCOSMOS 10 k Mocks

The mocks we use to calibrate and test our groupfinders are adapted from the COSMOS mock light cones (Kitzbichler & White 2007). These light cones are based on the Millennium DM-N-body simulation (Springel et al. 2005) that was run with the cosmological parameters $\Omega_m = 0.25$, $\Omega_{\Lambda} = 0.75$, $\Omega_b = 0.045$, $h = 0.73$, $n = 1$, and $\sigma_8 = 0.9$. The semianalytic recipes for populating the volume with galaxies in the light cones are that of Croton et al. (2006) as updated by De Lucia & Blaizot (2007). There are 24 independent mocks, each covering an area of 1.4 deg $\times$ 1.4 deg with an apparent magnitude limit of $r \leq 26$ and galaxies in the redshift range $z \lesssim 7$.

These light cones were adjusted to resemble the real 10 k sample as much as possible. First, a magnitude cut of $15 \leq i \leq 22.5$ was applied. However, the mean number of galaxies in the resulting mocks was about 5%–10% higher than in the zCOSMOS target catalog (i.e., a $1\sigma$–$2\sigma$ effect). To make the mocks more closely resemble the real data, we adjusted the magnitude cut in a redshift-dependent way so that the mean number of galaxies per unit redshift $dN_{gal}(z)/dz$ in the mocks was equal to the smoothed $N_{gal}(z)/dz$ of the zCOSMOS input target catalog (see Figure 1). Then, the spatial sampling completeness and the redshift success rate were simulated by removing galaxies from the mocks according to the probability that a galaxy with a certain position and redshift would have been observed in the 10 k sample. It should be noted that zCOSMOS is a slit-based survey. However, the bias against close neighbors—already small because of the multiple passes (up to 8 in the central region) across the field—is further mitigated by galaxies appearing serendipitously in slits targeted at other galaxies (see P. Kampczyk et al. 2009, in preparation). The small variation in sampling rate on these small scales, which is anyway well below the mean intergalactic separation in three-dimensional space, has been ignored in constructing the mocks. To further enhance the conformity with the 10 k sample, the redshift of each galaxy was perturbed by an amount drawn from a Gaussian distribution with standard deviation $\sigma_z = 100(1 + z)/c$ km s$^{-1}$.

### 2.3. Detectability of Groups

Since, according to our definition, a group is the set of galaxies occupying the same DM halo, we can only hope to detect those groups that host at least two galaxies in the 10 k sample. The collection of all these “detectable groups” constitutes the ideal (or “real”) group catalog. This is the best catalog that can be produced with the 10 k sample, and this is the catalog we aim to reconstruct with our groupfinder. Any DM halo hosting only a single zCOSMOS 10 k galaxy is not detectable and the corresponding galaxies will be termed “field galaxies.” For this reason, even the ideal group catalog that is detectable with the 10 k sample will not be a complete rendition of the true underlying group population in the COSMOS volume. Nevertheless, whenever we discuss the statistical properties of a
fraction of detectable groups in the "ideal" mocks as a function of DM halo mass. The left panel shows the redshift range $0.2 \leq z \leq 0.5$, and the right panel shows $0.5 \leq z \leq 0.8$. The upper panels show the number density of halos in the $10^k$ mocks (blue), in a purely $22.5$ magnitude-limited sample (red), and in total (black), and the lower panels show the fraction of halos in the $10^k$ sample (solid line) and in the magnitude-limited sample (dashed line) with respect to the total number of halos at a given mass. The shaded regions show the upper and lower quartiles of the fractions among the 24 mocks. For both redshift ranges, the $10^k$ sample was restricted to the central region of the survey.

group catalog, such as completeness or purity (see Section 3.2), these will be measured relative to this "ideal" group catalog, rather than the underlying population.

In a flux-limited survey such as zCOSMOS, the population of galaxies is observed changes with redshift, and the same will also therefore be true of the groups. For instance, for a group to be detectable at high redshift, it has to host at least two rather bright galaxies. Figure 2 shows the fraction of detectable groups in the mocks (i.e., in the "ideal" catalog in the previous paragraph) as a function of the halo mass in the two redshift bins $0.2 \leq z \leq 0.5$ and $0.5 \leq z \leq 0.8$. While in the lower redshift bin the sample should be complete down to $\sim 5 \times 10^{13} M_{\odot}$, this limit increases in the higher redshift bin to $\sim 2 \times 10^{14} M_{\odot}$. However, in both bins the bulk of the detectable halos are in the mass range $10^{12} M_{\odot} \lesssim M \lesssim 5 \times 10^{13} M_{\odot}$.

3. GROUP-FINDING METHOD

In this section, the different group-finding methods and the statistical properties of the resulting group catalogs are discussed. We have applied both the FOF and VDM algorithms to our sample. In this way, we are able to compare the resulting group catalogs obtained by the different methods and to investigate the robustness of the results.

3.1. The FOF and VDM Algorithms

3.1.1. FOF

The FOF algorithm is adopted from Eke et al. (2004). It has three free parameters: the linking length $b$, the maximum perpendicular linking length in physical coordinates $L_{\text{max}}$, and the ratio between the linking length along and perpendicular to the line of sight $R$. The exact meaning of these parameters becomes clear by regarding the linking criteria: consider two galaxies $i$ and $j$ with comoving distances $d_i$ and $d_j$, respectively. These two galaxies are assigned to the same group if their angular separation $\theta_{ij}$ satisfies

$$\theta_{ij} \leq \frac{1}{2} \left( \frac{l_{\parallel,i}}{d_i} + \frac{l_{\perp,i}}{d_j} \right)$$

and, simultaneously, the difference between their distances satisfies

$$|d_i - d_j| \leq \frac{l_{\parallel,i} + l_{\perp,i}}{2}.$$  

$L_{\perp}$ and $l_{\parallel}$ are the comoving linking lengths perpendicular and parallel to the line of sight defined by

$$l_{\perp} = \min\left[L_{\text{max}}(1+z), \frac{b}{\bar{n}^{1/3}} \right].$$

$$L_{\parallel} = R L_{\perp},$$

where $\bar{n}$ is the mean density of galaxies. Since the sample of galaxies is magnitude limited, the mean density of galaxies decreases with redshift leading to a steady increase of the mean intergalaxy separation with redshift. Eke et al. (2004) argued that scaling both $l_{\perp}$ and $l_{\parallel}$ with $n^{-1/3}$ will compensate for the magnitude limit and lead to groups of similar shape and overdensity throughout the survey. The free parameter $L_{\text{max}}$ has been introduced to avoid unphysically large values for $l_{\perp}$ at high redshifts where the galaxy distribution is sampled very sparsely. Since $L_{\text{max}}$ is measured in physical coordinates, $L_{\text{max}}(1+z)$ is the maximal comoving linking length perpendicular to the line of sight. Finally, the free parameter $R$ allows $l_{\perp}$ to be larger than $l_{\perp}$ taking into account the elongation of groups along the line of sight due to the fingers-of-God effect.

3.1.2. VDM

The VDM algorithm was adopted from Gerke et al. (2005) which was itself based on the method developed by Marinoni et al. (2002). This algorithm is more complicated than the FOF and has six free parameters instead of three. Basically one needs a full Voronoi–Delaunay tesselation of the input galaxy sample and the volumes of each Voronoi cell, The Voronoi–Delaunay tesselation was computed using Qhull (Barber et al. 1996) and the volumes of the Voronoi cells using the algorithm of Mirtich (1996).

The VDM algorithm can be divided into three phases: in Phase I, the galaxies are ordered in ascending order of Voronoi volumes. Then, the first galaxy in this sorted list is taken as a "seed galaxy" and a cylinder of radius $R_i$ and length $2L_i$ using comoving coordinates is placed around it such that the axis of the cylinder is directed along the line of sight. If there is no other galaxy inside this cylinder, the "seed galaxy" is

23 For a given set of sites in space, the "Voronoi cell" of a certain site consists of all points closer to this site than to any other site. Furthermore, two sites whose Voronoi cells share a common interface are called "Delaunay neighbors." The "Voronoi–Delaunay tesselation" for a given set of sites is the complete set of all its Voronoi cells and Delaunay neighbors. For more formal definitions and basic properties of Voronoi–Delaunay tesselations we refer to basic textbooks of geometry.

24 http://www.qhull.org
regarded as a field galaxy and one proceeds to the next galaxy in the list. If, however, there are other galaxies within the cylinder, Phase II starts. In this phase, a second cylinder with radius \( R_\text{II} \) and length \( 2L_\text{II} \) is defined and all galaxies inside this second cylinder directly connected to the seed galaxy or to its immediate Delaunay neighbors by means of the Delaunay mesh are assigned to the same group. The number of galaxies inside the second cylinder \( N_\text{II} \) is taken as an estimate of the central richness of the group. In Phase III, a third cylinder with radius \( R_\text{III} = r(\tilde{N}_\text{III})^{1/3} \) \( L_\text{III} = l(\tilde{N}_\text{III})^{1/3} f(z) \)

is defined, whereas \( r \) and \( l \) are two free parameters, \( \tilde{N}_\text{II} \) is the central richness corrected for the redshift-dependent mean density \( \tilde{n}(z) \), and \( f(z) \) is a function introduced to take into account that for a fixed velocity dispersion the length of the fingers of god in redshift space is a function of redshift. \( \tilde{N}_\text{II} \) and \( f(z) \) are given by

\[
\tilde{N}_\text{II} = \frac{\tilde{n}(z_{\text{ref}})}{\tilde{n}(z)} N_\text{II}
\]

and

\[
f(z) = \frac{s(z)}{s(z_{\text{ref}})}, \quad s(z) = \frac{1 + z}{\sqrt{\Omega_m(1+z)^3 + \Omega_\Lambda}},
\]

respectively, where \( z_{\text{ref}} \) is an arbitrary reference redshift chosen to be 0.5. In this third phase, again all galaxies within the third cylinder are assigned to the current group. After fixing \( z_{\text{ref}} \), six free parameters \( R_1, L_1, R_\text{II}, L_\text{II}, r, \) and \( l \) remain. The reader is referred to Table 1 for typical parameter sets for the two groupfinders.

It can be seen that both group-finding algorithms are somewhat arbitrary and neither is directly inked to the physical basis of a group, namely virialized motion within a common potential well. While it seems that the VDM algorithm is at least partly motivated by certain scaling relations for groups (Gerke et al. 2005), this is at the expense of simplicity, which is clearly the mark of the FOF algorithm.

### 3.2. Basic Statistical Quantities

In order to assess the performance of a groupfinder, realistic mock catalogs containing full information about the underlying DM halos and their properties are needed. In this section, we introduce some useful statistics to characterize the overall fidelity of the resulting group catalogs.

The fidelity of the group catalog can be assessed through comparing the “reconstructed” groups, obtained by running the groupfinder on the mock catalogs, to the “real” group catalog described above, i.e., the set of all DM halos in the mocks that contain, after the 10 k selection criteria have been applied, at least two galaxies. The comparison is therefore of two identical point sets, the galaxies in the mocks, whose points are grouped together in possibly different ways. This is schematically illustrated in Figure 3.

We follow here the definitions and notations of Gerke et al. (2005). The two big circles constitute two group catalogs.

![figure3](image-url)

**Figure 3.** Schematic illustration of comparing a reconstructed group catalog to a real group catalog as obtained from DM simulation. The left big circle constitutes the real group catalog and the right big circle the reconstructed group catalog. Each point displays a galaxy and the encircled points inside the big circles constitute groups. A group in the real (reconstructed) catalog may be associated with a group in the reconstructed (real) catalog (see the text for details). Such an association is indicated by an arrow pointing from the real (reconstructed) group to the reconstructed (real) group. If there is an arrow pointing from one group to another and also an arrow pointing backward, such an association is termed a “two-way match.” Otherwise it is just a “one-way match.” If more than one reconstructed group points to the same real group this is called “fragmentation,” if there is more than one real group associated with the same reconstructed group, this is called “overmerging.”
Each point corresponds to a galaxy of the input galaxy sample and the encircled galaxies belong to the same group. In the left-hand catalog are the “real groups” as given by the DM halos in the simulation, while in the right-hand catalog are the “reconstructed groups” as identified by our groupfinder. Some sort of measure is needed of how many reconstructed groups can be identified with real groups and how many real groups are recovered by our groupfinder. Following Gerke et al. (2005), we define the following terms.

1. Association. A group $i$ is associated with another group $j$ if group $j$ contains more than the fraction $f$ of the members of group $i$. For this association to be unique, it must hold $f \geq 0.5$. Throughout this paper, we set $f = 0.5$ as did Gerke et al. (2005).

2. One-way-match. If group $i$ is associated with group $j$, but group $j$ is not associated with group $i$ (illustrated by an arrow from group $i$ to group $j$).

3. Two-way-match. If group $i$ is associated with group $j$ and vice versa (illustrated by a double arrow).

While each group can only have a single, unique associated group (i.e., an arrow pointing away), it might well happen that a certain group is the associated group for many other groups (i.e., many arrows pointing toward it). We therefore have the following terminology.

1. Overmerging. If more than one real group is associated with the same reconstructed group.

2. Fragmentation. If more than one reconstructed group is associated with the same real group.

3. Spurious group. A reconstructed group which has no associated real group.

4. Undetected group. A real group that has no associated reconstructed group.

5. Group galaxy. A galaxy that belongs to a group.

6. Field galaxy. A galaxy not associated with any group.

With this terminology, the following statistical measures can be defined that together describe the overall fidelity of the reconstructed group catalog and thus its potential usefulness for quantitative analysis. Let $N_{\text{gr}}(N_{\text{real}})$ denote the number of real groups with $N_{\text{real}}$ members, and $N_{\text{gr}}(N_{\text{rec}})$ the number of reconstructed groups with $N_{\text{rec}}$ members. Then by

$$A[N_{\text{gr}}(N_{\text{real}}) \rightarrow N_{\text{gr}}(N_{\text{rec}})]$$

we denote the number of associations of real groups with $N_{\text{real}}$ members to reconstructed groups with $N_{\text{rec}}$ members. In the same way,

$$A[N_{\text{gr}}(N_{\text{rec}}) \rightarrow N_{\text{gr}}(N_{\text{real}})]$$

denotes the number of associations of reconstructed groups with $N_{\text{rec}}$ members to real groups with $N_{\text{real}}$ members. The analog notations for the numbers of two-way associations are

$$A[N_{\text{gr}}(N_{\text{real}}) \leftrightarrow N_{\text{gr}}(N_{\text{rec}})]$$

$$A[N_{\text{gr}}(N_{\text{rec}}) \leftrightarrow N_{\text{gr}}(N_{\text{real}})].$$

Note that the last two expressions are equivalent to each other. Then, with these notations we can formally introduce the “one-way completeness” $c_1(N)$ and the “two-way completeness” $c_2(N)$ by

$$c_1(N) = \frac{A[N_{\text{gr}}(N_{\text{real}}) \rightarrow N_{\text{gr}}(N_{\text{rec}})]}{N_{\text{real}}(N_{\text{rec}}) \geq N}.$$  

Analogously, we define the “one-way purity” $p_1(N)$ and “two-way purity” $p_2(N)$ as

$$p_1(N) = \frac{A[N_{\text{gr}}(N_{\text{rec}}) \rightarrow N_{\text{real}}(N_{\text{rec}})]}{N_{\text{rec}}(N_{\text{rec}}) \geq N}.$$  

$$p_2(N) = \frac{A[N_{\text{gr}}(N_{\text{rec}}) \leftrightarrow N_{\text{gr}}(N_{\text{real}})]}{N_{\text{rec}}(N_{\text{rec}}) \geq N}.$$  

The one-way “completeness” $c_1(N)$ is a measure of the fraction of real groups with $N$ or more members that are successfully recovered in the reconstructed group catalog, and the one-way “purity” $p_1(N)$ is a measure of the fraction of reconstructed groups with $N$ or more members that belong to real groups. The higher $c_1(N)$ the smaller the fraction of undetected groups $(1 - c_1(N))$, and the higher $p_1(N)$ the smaller the fraction of spurious groups $(1 - p_1(N))$. On the other hand, the smaller the ratios $c_2(N)/c_1(N) or p_2(N)/p_1(N)$ the more overmerging or fragmentation, respectively, is present. By definition the four quantities $c_1(N), c_2(N), p_1(N),$ and $p_2(N)$ all take only values between 0 and 1.

While Gerke et al. (2005) have introduced these four quantities $c_1, c_2, p_1,$ and $p_2$ globally for a group catalog including all groups, we have defined them to be functions of the number of members $N$ (“richness”). It will become clear below that investigating these statistics as a function of $N$ is very useful for improving the performance of a group catalog. Note that the argument $N$ always means “for groups with $N$ or more members” as is clear from their definitions, so for $N = 2$ the two definitions are identical. Throughout this paper we will always consider the set of groups down to a given richness-class $N$. So this convention eases the notation. It would, however, be straightforward to define the analog quantities in a noncumulative way.

While $c_1(N), p_1(N)$, etc., are statistical quantities on a group-to-group basis, statistical quantities on a galaxy-to-group basis may be useful as well. Therefore, following Gerke et al. (2005), we define the “galaxy success rate” $S_{\text{gal}}(N)$ and the “interloper fraction” $f_1(N)$ as

$$S_{\text{gal}}(N) = \frac{S_{\text{gal}}(N) \cap S_{\text{gal}}(N)}{S_{\text{gal}}(N)}$$

$$f_1(N) = \frac{S_{\text{gal}}(N) \cap S_{\text{field}}}{S_{\text{gal}}(N)},$$

where $S_{\text{real}}(N)$ is the set of galaxies associated with real groups of $N$ members, $S_{\text{rec}}(N)$ the set of galaxies associated with reconstructed groups of $N$ members, and $S_{\text{field}}$ is the set of real field galaxies. The square brackets $[\ ]$ here denote the number of elements in a set and the $\cap$ is the usual intersection from set theory. Thus, galaxy success rate $S_{\text{gal}}(N)$ is just the fraction of galaxies belonging to real groups of richness $\geq N$ that have ended up in any reconstructed group, and the interloper fraction $f_1(N)$ is the fraction of galaxies belonging to reconstructed groups of
richness $\geq N$ that are field galaxies (“interlopers”). Like $c_1(N)$, $p_1(N)$, etc., $S_{gal}(N)$ and $f_1(N)$ will also take values between 0 and 1.

It is well known (e.g., Frederic 1995; Gerke et al. 2005) that a perfect reconstructed group catalog is impossible to achieve and furthermore, that completeness and purity tend to be mutually exclusive. As would be expected, the higher the completeness, the lower the purity, and vice versa (see Figure 4). There is also a similar dichotomy between overmerging and fragmentation. Therefore, we introduce additional measures of “goodness”, which combine the statistics such as completeness and purity in a way that maximizing (or minimizing) them yields a sort of “optimal” group catalog. We formally define as (omitting the dependence of $N$ for the sake of clarity):

$$g_1 = \sqrt{(1 - c_1)^2 + (1 - p_1)^2}$$  \hspace{1cm} (19)

$$g_2 = \frac{c_2}{c_1} \frac{p_2}{p_1}$$  \hspace{1cm} (20)

$$g_3 = \sqrt{(1 - S_{gal})^2 + f_1^2}.$$  \hspace{1cm} (21)

The meaning of these quantities is as follows. Since a perfect group catalog features $(c_1, p_1) = (1, 1)$, i.e., entirely complete and absolutely pure, the reconstructed group catalog should come as close as possible to this point in the $c_1$-$p_1$ plane. So $g_1$ gives the distance to this optimal point in the $c_1$-$p_1$ plane and thus is a measure of the balance of completeness and purity. Then, a good group catalog should exhibit $c_1 \simeq c_2$ and $p_1 \simeq p_2$ meaning that essentially no overmerging and fragmentation is present in the catalog. Hence, $g_2$ measures the balance between overmerging and fragmentation and should also approach 1. Finally, $g_3$ is similar to $g_1$ but is on a galaxy-to-group basis instead of a group-to-group basis. As is clear from their definitions, these measures of goodness again take only values between 0 and 1. It is clear that $g_1$ and $g_3$ should be minimized, while $g_2$ should be maximized.

### 3.3. Optimization Strategy

Since there exists no single perfect reconstructed group catalog, one has to optimize the group-finding parameters, in principle, in a way that the resulting group catalog serves as well as possible the intended scientific purpose. However, as we will see, there seems to be a rather natural way to construct a group catalog that is useful for many different purposes. The only way to find such optimal parameters of a groupfinder is to run it on the mocks for different parameter sets, and to compare the resulting group catalogs by means of the statistics introduced in the previous section.

The completeness $c_1(8)$ and purity $p_1(8)$ of the reconstructed group catalogs, after running FOF and VDM over a large parameter space, are shown in Figure 4. It is obvious that the points do not extend arbitrarily close to the right upper corner (i.e., the perfect group catalog). The parameters $c_1(8)$ and $p_1(8)$ are in some sense anticorrelated. In fact, the cloud of points seem to feature a boundary toward high completeness and purity beyond which there is a region totally free of points. It is notable, how similar this boundary is for FOF and VDM approaches—clearly neither is markedly superior to the other. The same holds for the $g_2(8)$-goodness, color-coded in the figure, along this boundary region. These similarities between FOF and VDM are observed for all richness classes $N$. This indicates that this boundary is probably the limit of what can be achieved with a $z$COSMOS-10 k-like sample and does not depend on the choice of algorithm. This also suggests that the choice of a particular groupfinder such as FOF or VDM is less important than sometimes argued, although, as we will see, the properties of group catalogs obtained using the two groupfinders are not absolutely identical.

VDM, much more than FOF, also exhibits some scatter in the range given by $0.5 < c_1(8) < 0.85$ and $p_1(8) > 0.65$. The existence of such parameter sets is a natural side-effect of the relatively large number of free parameters of the VDM groupfinder resulting in many parameter combinations with obviously suboptimal properties in terms of $c_1(8)$ and $p_1(8)$. The extent of this scatter, of course, also depends strongly on the explored range of values in the parameter space. Since we are interested in parameter sets yielding simultaneously high completeness and high purity, we will only focus on the boundary mentioned above.

The challenge is to find the best group catalogs among those plotted in Figure 4, making the best compromise between $c_1$ and $p_1$. A natural choice is the point that lies closest to $(c_1, p_1) = (1, 1)$ indicated by the diamond. According to
Equation (19), this is the point where \( g_1 \) is minimal. We will refer to this parameter set as the “best \( g_1 \)-set.” It defines a circle around the upper right corner (dotted line) that is entirely empty of points.

In addition to minimizing \( g_1 \), one would prefer, of course, to simultaneously maximize \( g_2 \) and minimize \( g_3 \). In general, the best parameter sets for these three goodnesses will not coincide. Rather it turns out that the best \( g_2 \)-set lies usually at slightly higher completeness relative to the best \( g_1 \)-set (see triangles in Figure 4), while the best \( g_3 \)-set lies usually at slightly lower completeness (see squares in Figure 4). However, as is clear from Figure 4, the gradient of \( g_2 \) is rather shallow around the best \( g_1 \)-set and nearly maximal, so that the precise site of the optimal \( g_2 \)-set is not that important. The same holds for the gradient of \( g_3 \). Finally, it seems that the best \( g_1 \)-set is a good choice.

### 3.3.1. Multirun Procedure

Since \( c_1(N) \), \( c_2(N) \), etc., are functions of richness \( N \), one might wonder how the best \( g_1(N) \)-sets for different \( N \) are distributed in the \( c_1(8)–p_1(8) \) plane. This is shown in Figure 4 by the labeled points where the labels denote the corresponding \( N \). For FOF, the best \( g_1(N) \)-set is optimal for all \( N \geq 8 \) as well, while for \( N < 8 \) the optimal \( g_1(N) \)-sets reside at lower completeness. For VDM this is less obvious, but at least for \( N \geq 10 \) the best \( g_1(N) \)-sets seem to converge. In any case, it is clear that it is not possible to simultaneously optimize \( g_1(N) \) for all \( N \) with a single parameter set. If the parameter set is optimized for groups with \( N \geq 8 \), the resulting group catalog is very complete for groups with \( N < 8 \) but the purity starts to decrease severely for \( N < 5 \), and a lot of spurious small groups enter the catalog (see Figures 5 and 6). Since around \( \approx \) 80% of the groups have \( N < 5 \), this is unsatisfactory.

This suggests that the groupfinder should be run several times with different parameter sets, each time optimized for a different richness range. This is analogous to the “hot–cold” double pass approach often used with image detection algorithms such as SExtractor. We will refer to this approach as the “multirun procedure,” and it was implemented as follows.

1. The parameter set is optimized for the range \( N \geq 6 \), the groupfinder is run, and only those groups that are in this richness range are kept in the group catalog.
2. The parameter set is then optimized for groups with \( N = 5 \), the groupfinder is run again, and only groups with \( N = 5 \) that are not yet detected in the first step are added to the group catalog.
3. Repeat the previous step for \( N = 4 \).
4. Repeat the previous step for \( N = 3 \).
5. Repeat the previous step for \( N = 2 \).

In each step, only those groups are accepted which have not been found in an earlier step. It is better to work down in richness because the richer groups are more easily detected. The optimal parameter set in each step is basically just the best \( g_1 \)-set for the corresponding richness range. However, particularly in the first step, also other choices are possible. In fact, for VDM, we have chosen a special set for the first step since the best \( g_1(6) \)-set proved to be by no means optimal for \( N \geq 8 \). Table 1 gives the optimal parameter sets for FOF and VDM. Since there are some degeneracies between the parameters, there are no simple trends from step 1 to step 5 for the single parameters.

Figure 5 shows how the multirun procedure compares to the single run best \( g_1(8) \)-set. In the case of FOF, the completeness has slightly decreased for \( N \lesssim 5 \) compared to the single run, but the high completeness of the single run in this richness range comes at the cost of a low purity. In fact, for the multirun, the purity has increased for \( N \lesssim 5 \), and has become almost constant for all richness classes. Thus, the overall behavior of the completeness and purity is now more balanced.
For VDM, we observe a similar trend. Here, it is particularly evident that in a single run, even if optimized for $N \geq 8$, the completeness decreases for $N \gtrsim 6$. The multirun procedure can correct for this and still increase the purity for small groups.

While the overall statistics of the two multirun catalogs are similar, there are some minor differences. The overall behavior of the completeness and purity as a function of $N$ seems to be more balanced for FOF. Also the ratios $c_2/c_1$ and $p_2/p_1$ are more balanced for FOF, while for VDM, $c_2/c_1$ increases and $p_2/p_1$ decreases toward higher $N$. On the other hand, the total number of groups found with FOF is too high for $N \lesssim 3$, while for VDM, the number of reconstructed groups is too high for $N \gtrsim 5$ (Figure 6). All things considered, the multirun procedure works better with FOF than with VDM.

### 3.3.2. Combining FOF and VDM

With the FOF and VDM multirun group catalogs, there are now two catalogs available, obtained by different algorithms, and exhibiting similar purity and completeness. A comparison of the two catalogs on a group-to-group basis is shown in Figure 7. The red lines show the result for the real 10 k sample. An FOF group with $N \geq 2$ has a probability of being associated with a VDM group of $\sim 80\%$, increasing roughly linear with $N$ until it reaches $100\%$ for $N \geq 10$. On the other hand, the probability of any VDM group being associated with a FOF group is greater than $\sim 80\%$, and even higher than $\sim 90\%$ for $N \geq 8$. The reason that for $N \lesssim 4$ the VDM groups have a higher probability of being associated with the FOF groups than vice versa is due to the excess production of small groups in the FOF catalog. Furthermore, note that whenever a group with $N \geq 6$ has an associated group this association is a two-way association. Thus, the two catalogs, though not identical, contain mainly the same structures. Moreover, the real data agree very well with the mocks (black solid lines), if groups with $N > 20$ in the mocks are omitted (in the mocks there are too many of them, see Section 5.1). This shows that the groupfinders work indeed comparably on the real data as they do on the mocks.

Is there a way to combine the information in the two catalogs in order to obtain a single optimal group catalog? It seems natural to consider those group galaxies that were recovered by both groupfinders. We introduce a “galaxy purity parameter” (GAP) for each galaxy. The GAP is a flag indicating if a certain group galaxy is contained simultaneously in both catalogs. For a certain FOF group galaxy it is defined as follows.

1. If there is no VDM group containing this galaxy, it gets a GAP equal to 0.
2. If it is also contained in a VDM group, and the FOF group has a one-way match to this VDM group or this VDM group exhibits a one-way match to the FOF group, the galaxy gets a GAP equal to 1.
3. If it is contained in a VDM group, and the FOF group has a two-way match to this VDM group, the galaxy gets a GAP of 2.

Thus, we expect that the higher the GAP for a galaxy, the more reliable the detection, and the higher the probability that this galaxy is a real group galaxy and not an artifact introduced by one of the groupfinders. The GAP is a useful flag for excluding uncertain group members if needed, and defines more clearly the reliable core of a group.

Then, we can define two subsets, or “subcatalogs,” of the basic FOF catalog. The “one-way-matched” (1WM) subcatalog contains only FOF group galaxies with a GAP $\geq 1$. In a similar way, the “two-way-matched” subcatalog contains only group galaxies with a GAP $= 2$, i.e., all galaxies with a GAP $\leq 1$ become field galaxies. Note that we have defined the GAP, and thus the 1WM and 2WM, based on the FOF groups. They could, of course, also be defined based on the VDM groups. However, to obtain a single optimal group catalog, we have to choose between FOF and VDM. As discussed in the last section, though the multirun catalogs obtained by these groupfinders exhibit similar statistics, some (minor) properties are overall better for FOF. So we have decided the FOF catalog to be the basic catalog. The VDM catalog, by contrast, is therefore only used to determine the GAPs of FOF group members. Since the two subcatalogs preserve the group structure of the basic FOF catalog, this set of three group catalogs can be presented as one single big catalog with the GAP flags to indicate the increasing purity.

### 3.4. Results on the Mocks

In this section, we will summarize our findings and give a detailed statistical description of the FOF catalog with its two subcatalogs (1WM and 2WM).

The statistics of the merged catalogs in comparison with the reference FOF catalogs is shown in Figure 8 and for $N \geq 5$ in Table 2. The lines exhibit the mean among the 24 mocks and the error bars their scatter. The FOF basis catalog has a completeness $c_1 \approx 0.85$ almost not depending on the richness $N$ and a purity $p_1 \approx 0.78$ only weakly depending on $N$. Only for $N = 2$ there is a significant decrease in both completeness and purity. The corresponding statistics for the 1WM and 2WM subcatalogs have almost identical dependences on $N$ but, as expected, their $c_1$ is lower and $p_1$ higher.

It can be seen that the gain of the 2WM catalog compared to 1WM in terms of both purity or interloper fraction is much smaller than the deficit in terms of completeness and galaxy
success rate. This indicates that by keeping only group galaxies with a GAP = 2, many real group galaxies are removed, but only a relatively small number of interlopers are eliminated. By contrast, the gain in purity of the 1WM with respect to the reference FOF is quite comparable to the associated decrease in completeness. Thus, while the 1WM catalog is a useful construction, little is gained by the more restrictive 2WM catalog. In the remainder of this paper, we will mainly refer to the FOF and its 1WM subcatalog. We note that not only do the ratios $c_2/c_1$ and $p_2/p_1$ behave well as a function of $N$ for the three catalogs, but also $c_2/c_1 \simeq p_2/p_1$. This means that the contributions of overmerging and fragmentation are not only small, but are also well balanced.

So far, we have considered the statistics averaged over the whole redshift range, i.e., $0.1 \lesssim z \lesssim 1$. In Figure 9, the completeness (blue line) and the purity (red line) of the FOF catalog are shown as functions of redshift for several richness classes $N$. The curves are consistent with a relatively constant completeness and purity with redshift. Only the highest redshift bins for $N \lesssim 4$ show possibly a slight decrease. This emphasizes further the robustness of our catalog.

Figure 9 shows how the galaxy success rate $S_{\text{gal}}$ and the interloper fraction $f_I$ behave as a function of the normalized projected distance from the group centers. The distance variable $r$ is defined for each group galaxy as

$$r = \sqrt{\left(\frac{\theta_{\text{ra}}}{\Delta \theta_{\text{ra}}}\right)^2 + \left(\frac{\theta_{\text{dec}}}{\Delta \theta_{\text{dec}}}\right)^2}.$$ 

(22)
Similar definitions hold for groups as a function of $r \lesssim \text{galaxies as a function of separation from the cluster centers. It is clear that at to the 1WM catalog. The left upper panel shows the distribution of real group

where $r_f$ is its separation from the group center in $\alpha$, and $\Delta \theta_{\alpha}$ is the second moment in $\alpha$ among all members of this group. Similar definitions hold for $\theta_{\text{dec}}$ and $\Delta \theta_{\text{dec}}$. Only groups with three or more members are taken into account, since for groups with only two members $r$ becomes meaningless.

The left lower panel shows the galaxy success rate $S_{\text{gal}}$ as a function of $r$ from the real group centers. As one would expect, it increases toward the group centers. Fortunately, the group centers are also the region where most of the real group galaxies reside (left upper panel). Note that $S_{\text{gal}}$ can decrease, in principal, in two ways: first of all, by failing to identify certain real group galaxies in successfully detected real groups, and second, by failing to detect a real group at all. The small deficit in $S_{\text{gal}}$ for $r \lesssim 1$ is due to the second reason, while the first reason becomes more important with increasing $r$.

In the lower right panel, the interloper fraction $f_I$ is plotted as a function of $r$, where $r$ is now related to the centers of the reconstructed groups. As expected, the interloper fraction shows the opposite behavior as a function of $r$. However, the difference in $f_I$ between near and far galaxies from the group centers is less strong than for $S_{\text{gal}}$. For small $r$, the most important contribution to $f_I$ comes from spuriously detected groups with three members.

Finally, Figure 6 shows the numbers of reconstructed groups relative to the number of real groups. As was already mentioned, the mean difference between the number of reconstructed FOF groups and the number of real groups exceeds the uncertainty expected by cosmic variance from mock to mock for $N \lesssim 5$, while the groups of the 1WM subcatalog are well within this region.

According to the statistics discussed in this paragraph, particularly in Figure 2, it became clear that the FOF group catalog along with its 1WM subcatalog has the potential to be useful for many different applications such as galaxy evolution studies, group statistics, or gravitational lensing. For example, if one aims to study the evolution of galaxies in groups, a high purity and a low interloper fraction are desirable, so the 1WM catalog is probably appropriate. On the other hand, in order to have a relative pure sample of field galaxies, galaxies not contained in the basic FOF catalog should be selected. Generally, it holds that whenever small groups, number of groups, or purity of the group sample is important, the 1WM catalog is to be preferred to the FOF catalog.

3.5. Comparison with DEEP2

For DEEP2, Gerke et al. (2005) optimized their VDM groupfinder in order to obtain the correct number of reconstructed groups $N^i_{\text{VDM}}(\sigma, z)$ as a function of velocity dispersion $\sigma$ and redshift. As result, they present two group catalogs: an “optimal” catalog and one with maximized purity. Since Gerke et al. (2005) did not treat completeness and purity as a function of richness $N$, all their statistics correspond to $N \geq 2$.

The statistics for their optimal parameter set are $c_1 = 0.782 \pm 0.006$, $p_1 = 0.545 \pm 0.005$, $S_{\text{gal}} = 0.786$, and $f_I = 0.458 \pm 0.004$. The ratios between the two-way and the one-way quantities are therefore $c_2/c_1 = 0.919$ and $p_2/p_1 = 0.987$. So in comparison with our own FOF $N \geq 2$ statistics, their completeness $c_1$ and galaxy success rate $S_{\text{gal}}$ are $\sim 3\%$ and $\sim 6\%$ lower, respectively, while their purity $p_1$ is $\sim 17\%$ lower, and their interloper fraction $f_I \sim 56\%$ higher.

We conclude that, compared with the DEEP2 “optimal” group catalog, the performance of our FOF group catalog is very high. Moreover, it would be very interesting to compare the statistics for the higher richness classes as well. Since Gerke et al. (2005) optimized their catalog using all groups with $N \geq 2$ their catalog should be optimal regarding the $N \geq 2$ statistics. But, in contrast to a multirun catalog, this might not be the case for the higher richness statistics, since the $N \geq 2$ statistics are actually dominated by 2-member groups being by far the most abundant. This suggests that the relative superiority of our FOF catalog over the DEEP2 catalog could be even higher for the higher richness classes.

4. THE REAL DATA 10 k GROUP CATALOG

In this section, the real data 10 k group catalog is presented. It is given by means of the Tables 3 and 4. Table 3 is a list of all groups along with their properties, and Table 4 is a list of all group galaxies. The group galaxies are associated with their group by means of the unique group-ID. The galaxy-IDs refer to the 10 k catalog published by S. J. Lilly et al. (2009, in preparation).

4.1. Group Purity Parameter

Since we are presenting the FOF catalog along with its two subcatalogs, defined by the GAP parameter in the final column, any group property can, in principle, be calculated for all three catalogs. For instance, it is possible to assign to each group three observed richnesses $N$. To avoid confusion and to keep the discussion simple, all group properties given in Table 3 correspond to the basic FOF catalog. In order to quantify the number of 1WM galaxies in a certain group, we introduce the group purity parameter (GRP$_i$) for $i = 1, 2, 3$ defined by the fraction of FOF members having a galaxy purity parameter $\text{GAP} \geq i$. For $i = 1$ this is the fraction of FOF members that are also 1WM members, and for $i = 2$ that are also 2WM members. Note that if the GRP$_i$ is zero, then there is no association between the FOF group and a VDM group.
The statistics of the number of groups and the GRP<sub>1</sub> are summarized in Table 5. The basic FOF catalog contains 800 groups with $N \geq 2$, 102 groups with $N \geq 5$, and 23 groups with $N \geq 8$. Over 80% of the groups with $N \geq 2$ have a GRP<sub>1</sub> greater than zero, i.e., these groups have at least one group galaxy that was independently recovered by both FOF and VDM. For the groups with $N \geq 5$, the number of groups with GRP<sub>1</sub> $\geq 0$ rises to 95%, and for those with $N \geq 8$ it is 96% (22 out of 23). Figure 7 shows the comparison between the real data FOF and VDM catalogs.

The mean GRP as a function of richness $N$ is given in Figure 11. The blue solid line shows the mean GRP<sub>1</sub> taking into account all groups with $N \geq N$. There is a slight and noisy rise from about 0.8 for $N \geq 2$ to 0.9 for $N \geq 9$ due to the fact that the fraction of groups with GRP<sub>1</sub> equals zero is slightly bigger for smaller $N$. On the other hand, the dashed blue line shows the mean GRP<sub>2</sub> taking into account only groups with a nonzero GRP<sub>1</sub>, i.e., only groups simultaneously found by both groupfinder. For these groups, the GRP<sub>1</sub> is slightly decreasing since for bigger groups it becomes easier for the two groupfinders to disagree on one or two galaxies in the outskirts of the group. The red lines in Figure 11 show the same quantities for GRP<sub>2</sub>.

4.2. Corrected Richness $N_{\text{corr}}$

The distribution of FOF groups as a function of redshift for three richness classes $N$ is shown in Figure 12. Comparing the black histograms (groups) with the red dashed lines (all galaxies) it is clear that the number of groups at a given redshift scales with the number of galaxies at the same redshift. This is basically true for all richness classes although for the richest $N \geq 8$ there is a lack of groups at redshifts $z \gtrsim 0.5$. In the framework of the hierarchical cold dark matter (CDM) structure formation scenario we expect the cluster mass function to grow with time (for a review see Voit 2005). This growth should be reflected in the decrease of the number of groups of a given richness with redshift.

In order to address this question, it is necessary to correct the observed richness of a cluster to produce an intrinsic richness

The table is available in its entirety in a machine-readable form in the online journal. A portion is shown here for guidance regarding its form and content.

| Group ID | $N_a$ | $\alpha$ | $\delta$ | $z$ | $M_{\text{fudge}}$ | GRP<sub>1</sub> |
|----------|------|--------|--------|----|-----------------|-------------|
| 0        | 10   | 150.0087 | 2.0287 | 0.0788 | 409 | 8.20e12 | 0.9 |
| 1        | 7    | 149.4817 | 2.5073 | 0.0919 | 393 | 9.58e12 | 1  |
| 2        | 20   | 150.3004 | 2.4489 | 1.2311 | 442 | 6.09e13 | 0.95 |
| 3        | 6    | 150.3444 | 2.1544 | 0.1222 | 0   | 1.13e13 | 1  |
| 4        | 14   | 149.8568 | 1.8151 | 0.1243 | 532 | 1.92e13 | 0.93 |
| 5        | 6    | 149.7238 | 2.399 | 0.1252 | 0   | 1.23e13 | 1  |
| 6        | 6    | 150.2824 | 2.1531 | 0.1686 | 69  | 5.98e12 | 0.5 |
| 7        | 9    | 150.078  | 2.2136 | 0.1865 | 242 | 2.18e13 | 1  |
| 8        | 12   | 150.1122 | 2.3564 | 0.2208 | 596 | 2.71e13 | 0.92 |
| 9        | 10   | 150.4526 | 2.6799 | 0.2179 | 768 | 2.83e13 | 1  |
| 10       | 6    | 150.2371 | 1.9404 | 0.2188 | 238 | 1.13e13 | 1  |
| 11       | 6    | 150.2304 | 2.5608 | 0.2207 | 530 | 2.29e13 | 0  |
| 12       | 6    | 150.1636 | 2.0342 | 0.2208 | 355 | 1.35e13 | 1  |
| 13       | 8    | 150.2494 | 2.6574 | 0.2672 | 403 | 3.85e13 | 1  |

Notes.
- a Number of groups.
- b Fraction of groups with a group purity parameter (GRP<sub>1</sub>) larger than zero.

| Galaxy-ID | Group-ID | $N$ | $\alpha$ | $\delta$ | $z$ | GAP<sup>a</sup> |
|-----------|----------|----|--------|--------|----|-------------|
| 81878     | 0        | 150.0065 | 2.0067 | 0.0785 | 2  |
| 81888     | 0        | 150.0365 | 2.0249 | 0.0794 | 2  |
| 81934     | 0        | 150.0241 | 1.9687 | 0.0799 | 2  |
| 81935     | 0        | 150.0239 | 2.0727 | 0.0799 | 2  |
| 81982     | 0        | 150.0134 | 2.0296 | 0.0791 | 2  |
| 81903     | 0        | 149.9989 | 1.9858 | 0.0805 | 0  |
| 819041    | 0        | 149.9984 | 2.0351 | 0.0789 | 2  |
| 819060    | 0        | 149.9912 | 1.9912 | 0.0797 | 2  |
| 819118    | 0        | 149.9724 | 2.1054 | 0.0781 | 2  |
| 819133    | 0        | 149.9681 | 2.0673 | 0.0779 | 2  |
| 842033    | 1        | 149.4897 | 2.5164 | 0.0913 | 2  |
| 842048    | 1        | 149.4844 | 2.4991 | 0.0907 | 2  |
| 842049    | 1        | 149.4839 | 2.5211 | 0.0915 | 2  |

Notes.
- a Galaxy Purity Parameter (see Section 3.3.2).

Figure 11. Mean GRP as a function of observed richness $N$. The blue solid line shows the GRP<sub>1</sub> and the red solid line the GRP<sub>2</sub>. The dashed lines show the corresponding GRP<sub>i</sub>, $i = 1, 2$, by taking into account only the groups with a nonzero GRP<sub>1</sub>.

Table 5 Number of Groups

| $\geq N$ | $N_a$ | $f(\text{GRP1} > 0)$ | (GRP<sub>1</sub>) |
|---------|------|---------------------|-----------------|
| 2       | 800  | 0.82                | 0.80 |
| 3       | 286  | 0.86                | 0.81 |
| 4       | 150  | 0.95                | 0.88 |
| 5       | 102  | 0.95                | 0.88 |
| 6       | 59   | 0.95                | 0.87 |
| 7       | 36   | 0.94                | 0.86 |
| 8       | 23   | 0.96                | 0.88 |
| 9       | 17   | 1.00                | 0.93 |

Notes.
- a Number of groups.
- b Fraction of groups with a group purity parameter (GRP<sub>1</sub>) larger than zero.
that is redshift independent. We therefore introduce the corrected richness \( N_{\text{corr}} \), correcting the observed richness \( N \) for spatial sampling rate and redshift success rate, and considering for each group only the number of members brighter than a given absolute magnitude limit \( M_{b,\text{lim}}(z) \), i.e., for each group

\[
N_{\text{corr}}(M_{b,\text{lim}}(z)) = \sum_i \frac{1}{C_{\alpha,i} C_{\text{rsr},i}},
\]

where the sum is over the members of the group with \( M_b \leq M_{b,\text{lim}}(z) \), and \( C_{\alpha,i} \) and \( C_{\text{rsr},i} \) are the sampling rate and the redshift success rate, respectively, for the galaxy \( i \). The redshift dependence of the absolute magnitude limit is always taken to be \( M_{b,\text{lim}}(z) = M_{b,\text{lim}} - z \), whereas the subtraction of the redshift is to account approximately for the luminosity evolution of the galaxies. So \( N_{\text{corr}} \) can simply be characterized by \( M_{b,\text{lim}} \) being the absolute magnitude limit at redshift zero. Absolute magnitudes were obtained by means of standard multicolor spectral energy distribution (SED) fitting using an updated version of the ZEBRA code (Feldmann et al. 2006; P. Oesch et al. 2009, in preparation).

If we denote the actual number of group members brighter than \( M_{b,\text{lim}}(z) \) in a real group in the mocks (without the spatial or redshift sampling rates) by \( N_{\text{true}}(M_{b,\text{lim}}) \), then we find that, for reconstructed groups exhibiting a two-way match to real groups, the estimated \( N_{\text{corr}}(−20) \) exhibit a relatively large scatter (\( \pm 50\% \)) compared with \( N_{\text{true}}(−20) \) of the corresponding real groups. Furthermore, \( N_{\text{corr}}(−20) \) on average overestimates \( N_{\text{true}}(−20) \) by about 50%–100% depending on \( N \). This is because (1) for most groups we are in the low number regime, (2) the sampling rate in the 10 k sample is rather low (so the corrections are big and noisy), (3) groups with no galaxy brighter than \( M_{b,\text{lim}}(z) \) cannot be corrected for sampling rate at all, and (4) the reconstructed groups are affected by interlopers.

One should therefore be cautious in interpreting \( N_{\text{corr}} \) as the actual richness of the groups. Nevertheless, \( N_{\text{corr}}(−20) \) shows a relatively tight correlation with the estimated halo mass \( M_{\text{fudge}} \) (see Section 4.4), even for \( N \gtrsim 2 \), as is shown in Figure 13 and thus is still a useful quantity. The analysis of the redshift distribution for groups with a given \( N_{\text{corr}}(−20) \) is performed in Section 5.2.

### 4.3. Velocity Dispersion Estimation

The corrected richness \( N_{\text{corr}} \) discussed in the last section is probably the simplest and most straightforward characterization of a group. However, there are other characterizations of groups which may be more directly useful from a physical point of view such as velocity dispersion \( \sigma \) or dynamical mass \( M \). Since most of our groups have richness \( N \lesssim 10 \), we are in a low number regime, where the estimation of both velocity dispersion and mass is nontrivial.

According to Beers et al. (1990) the best estimators for velocity dispersion in groups with few members are the gapper estimator and the simple standard deviation. On the other hand, the biweight estimator seems to work very well on a large range of richness classes \( N \) except for \( N \lesssim 20 \) where its performance is lower but still sufficient. For comparison, we have implemented
all three estimators and none of them is significantly superior
to the others when applied to the mocks, and so we will stick to
the gapper estimator since it is the most commonly used among
the three.

The implementation for a group with \( N \) members is as follows.
First of all, for each group member \( i \) we computed the redshift
difference \( d z_i \) with respect to the mean group redshift \( z_{gr} \). Then
these redshift differences were converted into velocities by
\[
dv_i = c \frac{dz_i}{1 + z_{gr}}
\]
with \( c \) being the speed of light. Then after sorting the velocities
\( dv_i \) in ascending order, the gapper estimate is given by
\[
\sigma_{\text{gap}} = \frac{\sqrt{\pi}}{N(N - 1)} \sum_{i=1}^{N-1} w_i g_i,
\]
whereas the weights \( w_i \) and the gaps \( g_i \) are defined by
\[
w_i = i(N - 1) \\
g_i = dv_{i+1} - dv_i
\]
for \( i = 1, \ldots, N - 1 \). However in order to have a realistic
estimate of the velocity dispersion of our group we have to
correct \( \sigma_{\text{gap}} \) for our redshift uncertainty \( \sigma_z \) of roughly
100 km s\(^{-1}\). This is done by
\[
\hat{\sigma} = \sqrt{3} \sqrt{\sigma^2_{\text{gap}} - \sigma^2_z},
\]
where \( \hat{\sigma} \) is the final estimate of the velocity dispersion \( \sigma \). The
factor \( \sqrt{3} \) converts the line of sight velocity dispersion to the
three-dimensional velocity dispersion. If \( \sigma_z \) is larger than \( \sigma_{\text{gap}} \)
we set \( \hat{\sigma} \) formally to zero.

Since the COSMOS light cones (Kitzbichler & White 2007) provide only the “virial velocity”\(^{25} v_{\text{vir}} \) of the DM halos
and not directly the “velocity dispersion” \( \sigma \), we cannot precisely
estimate the uncertainty of the estimated \( \hat{\sigma} \) for a group. But
comparing \( \hat{\sigma} \) to \( v_{\text{vir}} \) should provide an upper limit to the
uncertainty. To take into account the influence of interlopers on
\( \hat{\sigma} \), we considered the estimated velocity dispersion of
reconstructed groups exhibiting a two-way match with real
groups (wrongly detected groups do not exhibit a meaningful
velocity dispersion).

We find that for \( N \geq 5 \) the ratio between the median
virial velocity \( v_{\text{vir}} \) and \( \sigma \) remains roughly constant for \( \sigma \gtrsim
350 \) km s\(^{-1}\), and exhibits an error of about 25% (upper and lower
quartile; Figure 14). Note that the estimated \( \sigma \) do not need to fall
exactly on the 45° line, since \( \sigma \) and \( v_{\text{vir}} \) are not exactly the
same quantities. For \( \sigma \lesssim 350 \) km s\(^{-1}\) the estimated velocity
dispersion \( \hat{\sigma} \) is biased to lower values due to the subtraction in
Equation (28). On the other hand, for \( N < 5 \), the correlation
between \( \hat{\sigma} \) and \( v_{\text{vir}} \) is very weak, so that the \( \hat{\sigma} \) for these richness
classes contains almost no information. Hence, we have decided
to assign no estimated velocity dispersion to groups with \( N < 5 \)
in Table 3.

Note that applying the velocity dispersion estimation to the
real groups instead of the reconstructed groups does not
significantly alter these results. Even estimating the velocity
dispersion for the real groups in the 10 k mocks taking into
account all galaxies down to \( r \lesssim 26 \) still yields a scatter of
about 10%–15%.

\(^{25}\) In the COSMOS light cones, the virial velocity is simply defined by
\( v_{\text{vir}} = \sqrt{G M_{200}/r_{200}} \), whereas \( G \) is the gravitational constant, and \( M_{200} \)
and \( r_{200} \) are the virial mass and the virial radius, respectively, related by
\( M_{200} = 4/3 \pi \rho_{c} r_{200}^{3} \), whereas \( \rho_{c}(z) \) is the critical density of the
universe at the redshift of the halo.

![Figure 14](image_url)

**Figure 14.** Correlation between the estimated velocity dispersions \( \hat{\sigma} \) of groups with \( N \geq 5 \) and the virial velocities \( v_{\text{vir}} \) of the DM halos. Each point displays a reconstructed group exhibiting a two-way match to a real group whose DM halo yields \( v_{\text{vir}} \). It is obvious that for \( \sigma \lesssim 350 \) the estimated velocity dispersion is underestimating the virial velocity.

### 4.4. Estimation of Dynamical Mass

Estimating the dynamical mass of the underlying DM halo
of a group is even more difficult than estimating the velocity
dispersion. The simplest method for the estimation of dynamical mass is by using some form of the virial theorem. The standard
relation is (e.g., Eke et al. 2004)
\[
\hat{M} = A \frac{\hat{\sigma}^2 r_{\perp}}{G},
\]
where \( A \) is a constant depending on the mass distribution of the
halo (e.g., geometry, concentration, etc.), \( \hat{\sigma} \) the estimated
velocity dispersion, and \( r_{\perp} \) is some estimate of its projected
radius. Heisler et al. (1985) discuss four simple mass estimators,
each being only a function of the projected distances and radial
velocities of the group galaxies with respect to the group center.
In applying them to the reconstructed groups in the mocks,
none of them works substantially better than the simple relation
in Equation (29) and all show a similar behavior, so we consider
only the standard virial theorem.

To use the estimator in Equation (29), the constant of
proportionality \( A \) needs to be calibrated properly. Doing this
with the mocks and using an appropriate estimation for the
projected radius, we find a similar behavior for the estimated
masses like for the velocity dispersion. For \( N \lesssim 5 \) there is
only a very weak correlation between the estimated mass and
the actual mass of the underlying DM halo. For \( N \gtrsim 5 \) there is
a correlation, but only for \( \hat{M} \gtrsim 5 \times 10^{13} M_{\odot} \), with an
error (upper and lower quartiles) of roughly a factor of 2
with respect to the median. Since these mass estimates would
be of relatively limited use and since the mocks are needed for
calibration anyway, we have instead pursued another approach.

It turns out that using observed richness \( N \), corrected for
sampling and redshift success rate, and redshift \( z \) as proxy for
the mass and calibrating them with the mocks works rather well.
The mass for a group with observed richness \( N \) and redshift \( z \) is
then simply given by

\[ M_{\text{fudge}} = \langle M_{\text{halo}}(\bar{N}, z) \rangle, \]  

(30)

where \( M_{\text{halo}}(\bar{N}, z) \) denotes the mass of a halo at redshift \( z \) containing \( \bar{N} \) galaxies, \( \bar{N} \) is the observed richness of the group corrected for sampling and redshift success rate, and the angle brackets denote the average over the halos in the 24 mocks. We will denote this mass as “fudge mass” to indicate that it is calibrated with the mocks.

The fudge masses of the reconstructed groups with \( N \geq 5 \) exhibiting a two-way-match to their real groups are shown in Figure 15. In contrast to the velocity dispersion estimates, there is no bias for small masses. The error for the masses (upper and lower quartiles) is about 50%. Furthermore, the masses are also defined for small groups, whereas the upper quartile increases toward 100% for \( N = 2 \). The lower quartile does not change significantly.

4.5. Manual Intervention: The Example of a Supergroup at \( z = 0.22 \)

After applying our group-finding procedure to the real 10 k sample, we encountered a huge structure, which resisted to yield even roughly consistent results between FOF and VDM. We mention this particular case, because it illustrates some of the weaknesses of our adopted groupfinder, and finally required a special treatment. It was already mentioned by Finoguenov et al. (2007) and is probably an example of a “supergroup,” where several smaller groups are just about to merge (Smolčić et al. 2007). The redshift of the system is about \( z \sim 0.22 \). An example of such a supergroup in another field at \( z = 0.37 \) is given by Gonzalez et al. (2005) and Kautsch et al. (2008).

The projected galaxy distribution of this structure is exhibited in Figure 16. The upper left panel shows the group assignment of the multirun FOF catalog, and the upper left panel the group assignment of the multirun VDM. Each group is denoted by a symbol (e.g., square, triangle) of a particular color, and field galaxies by black points. This example of the supergroup gives us some interesting insights concerning the group-finding procedure.

This extended structure exhibits the main potential problems of both the FOF and VDM algorithms. The FOF algorithm connected practically all the galaxies in this supergroup, without distinguishing between different subgroups. This behavior is well known for FOF, and it happens in particularly dense regions such as this. The problem is that any single galaxy between two of these subclusters will act as a bridge for the FOF algorithm to connect the two clusters. The VDM is more successful in distinguishing different substructures, but nevertheless fails to do a perfect job. A casual glance suggests that the “green square” VDM cluster in fact consists of two independent subgroups (consistent with the X-ray contours). Furthermore, the “red triangle” VDM group exhibits two outliers to the South, which almost certainly do not belong to this group. The occurrence of such outliers is not uncommon in VDM groups. It is related to the fact that in the VDM groupfinder every second-order Delaunay neighbor in the second cylinder is accepted as group member and that the second cylinder is usually much bigger than the third cylinder (see Section 3.1.2).

Since we have accepted the FOF catalog as the basis catalog, and since this supergroup is the only case where FOF is in such obvious disagreement with VDM, we decided to just correct this single structure manually after visual inspection. The final result is shown in the lower panel of Figure 16. The manually created groups by this intervention are group No. 8 and Nos. 795–799. Although the manual assignment of galaxies to subgroups is somewhat arbitrary, looking in redshift space (and not only at the projected galaxy distribution) the eye recognizes quite well different substructures. This example emphasizes how important precise redshift information is. Even if it had been possible to recognize this huge overdensity with precise photo-z, it would not be possible to disentangle the more subtle substructure reliably. This is illustrated best by the “blue upward triangle” and the “brown downward triangle” groups overlapping in projection (see lower panel of Figure 16).

5. COMPARISON WITH THE MOCKS AND 2DFGRS

In this section, we will compare our group catalog with the mocks. Since zCOSMOS was designed to have a similar survey design as the 2 Degree Field Galaxy Redshift survey (2dfGRS; Colless et al. 2001; see Lilly et al. 2007), albeit at higher redshifts, we also want to compare our group catalog to the 2PIGG group catalog (Eke et al. 2004) of 2dfGRS to have a reference point in the local universe. The 2PIGG catalog is particularly appropriate for comparison since it was obtained by essentially the same FOF algorithm we have adopted.

5.1. Number of Groups as a Function of \( N \)

The most straightforward way to compare the real data with the mocks is to compare the number of 10 k groups with the number of reconstructed groups in the mocks as a function of observed richness \( N \). This is shown in Figure 17. The number of 10 k groups is in good agreement with the number of reconstructed groups in the mocks. It seems that for \( N \lesssim 6 \) there is a slight excess of 10 k groups relative to the reconstructed groups. However, this excess is not significant.

More significant is the fact that for \( N \geq 20 \) there are significantly more groups in the mocks than in the real data.
While in the 10 k sample there is one group in this range (group No. 2 with $N = 20$)\textsuperscript{26}, the median number of reconstructed groups with $N \geq 20$ in a 10 k mock is 5 with upper and lower quartiles of 6 and 3, respectively. These groups are distributed in the redshift range $0.1 \lesssim z \lesssim 0.7$. Even groups with $N > 50$ should not be exceptional—on average there are $\sim 0.5$ of these per mock.

These huge groups are not an artifact of our reconstructed groups, but are also present in the real group catalog. More than 80% of the reconstructed groups with $N \geq 20$ exhibit a two-way match to a real group, as one would expect from Figure 8, and their mean $\text{GRP}_1$ is about 0.9. So we conclude that the lack of big groups in the 10 k sample is probably real and not due to some problem with the groupfinder.

5.2. Fraction of Galaxies in Groups

A quantity that is closely related to the number of groups in a catalog is the fraction of galaxies in the sample that are placed in groups. This fraction is shown as a function of redshift in Figure 18 for $N \geq 2$ and $N \geq 5$ in the central region. If the galaxies in the mocks associated with groups with $N \geq 20$ are not considered as group galaxies (solid blue and black line)—since we have shown that there are far too many of these groups in the mocks—the overall behavior of the fractions in the 10 k sample (red line) match quite well those of the reconstructed groups or real groups, at least in the redshift range $0.1 \lesssim z \lesssim 0.5$. If the galaxies in groups with $N \geq 20$ are treated as normal group galaxies (dashed blue and black line), the fraction of group galaxies in the mocks is too high, as expected.

Noticeable is the lack of group galaxies in the 10 k sample at redshift $z \sim 0.55$ and the excess at redshift $z \sim 0.9$, especially for $N \geq 2$. The lack of group galaxies at $z \sim 0.55$ coincides with a big underdensity in the 10 k galaxy sample and is clearly visible in Figure 12. The origin of the excess of group galaxies at high redshift is less clear. While there are single mocks with a deviation at $z \sim 0.55$ similar to the lack of group galaxies in the 10 k sample, none of the mocks approach the excess of group galaxies at redshift $z \sim 0.9$. These underdense and overdense regions are clearly seen in the overall galaxy density field constructed by Kováč et al. (2009).

The decline of group galaxies with redshift has two reasons: first of all, there are fewer groups at high redshift, as expected from the hierarchical growth of structure at these scales, and second, the fraction of detectable groups decreases with redshift, since the galaxy density decreases and so it becomes more and more improbable to observe two galaxies residing in the same DM halo. The second of these has been already discussed in Section 2.3 (see Figure 2), so we focus here mainly on the first reason which is demonstrated in Figure 19. Here the fraction of galaxies in groups is shown as a function of $N_{\text{corr}}\left(\sim 20\right)$, and all galaxies samples are chosen to be volume limited with respect to $M_{b, \text{lim}}(z)$. The solid black line exhibits the fraction of 10 k group galaxies in the redshift bin $0.2 \lesssim z \lesssim 0.5$, and the dashed black

\textsuperscript{26} Even if we regarded the supergroup in Section 4.5 as a single group with $N > 20$, the 10 k group catalog would still contain far fewer big groups than in most of the mocks.

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**Figure 16.** Group No. 8 in the uncorrected group catalog has been manually split up into several groups (No. 8, Nos. 795–799), because the FOF as well as the VDM method failed (see the text). Upper left panel shows the initial FOF groups, the upper right panel the initial VDM groups, and the lower panel the FOF groups after manual intervention. The black points denote field galaxies, and the other symbols (squares, triangles, etc.) are group galaxies, whereas each group has its own symbol and color. The blue contour exhibits the X-ray emission of the supergroup as observed with XMM-Newton (Finoguenov et al. 2007; A. Finoguenov et al. 2009, in preparation).
Figure 17. Number of groups $N_{tr}$ as a function of observed richness $N$. The upper panel shows the absolute number of groups, whereas the red lines correspond to the 10k groups, and the blue lines to the reconstructed groups in the mocks. The solid lines correspond to FOF groups, and the dashed lines to the 1WM groups. The error bars correspond to the real scatter among the 24 mocks. The gray shaded area exhibits the cosmic variance of real groups in the mocks among the 24 mocks. The lower panel shows the abundance of groups relative to the reconstructed FOF groups, whereas all symbols are the same as in the upper panel.

Figure 18. Fraction of galaxies in groups in the central region. The red solid line shows the fraction of galaxies in groups for the 10k catalog. The black dashed line shows the mean fraction of galaxies in real groups in the mocks and the green dashed line the mean fraction of galaxies in reconstructed groups. If only galaxies in groups with $N \leq 20$ are considered as group galaxies, the results are the solid black and green line, respectively. The error bars show the scatter among the 24 mocks.

Figure 19 shows clearly a decline of the fraction of group galaxies with redshift. Since $N_{corr}$ correlates fairly well with mass (see Figure 13), this decline can straightforwardly be interpreted in terms of growth of structure as expected in a hierarchical structure formation scenario (Voit 2005). In fact, using $M_{b,\text{lim}} = -20$ as absolute magnitude threshold to estimate $N_{corr}$ our sample is volume limited up to $z \sim 0.9$, and we have checked with the mocks that we do not loose groups due to detectability problems in this sample.

6. SUMMARY

The aim of this paper was to create a group catalog out of the spectroscopic zCOSMOS 10 k sample, to enable investigations of the galaxy population in groups over the redshift range $0.1 \lesssim z \lesssim 1$. The basic group-finding method was to use an FOF and a VDM groupfinder to identify galaxy overdensities in redshift space without regard to individual galaxy properties, using the precise $\sigma \sim 100$ km s$^{-1}$ velocities available from zCOSMOS. The performance of both FOF and VDM groupfinders was extensively tested using realistic mock spectroscopic samples generated from the COSMOS mock light cones (Kitzbichler &
Figure 19. Fraction of galaxies in groups as a function of $N_{\text{corr}} (\geq 20)$ in volume-limited samples. The solid black line shows the fraction of the 10 k group galaxies in the redshift bin $0.2 \leq z \leq 0.5$, and the dashed black line the fraction in the redshift bin $0.5 \leq z \leq 0.8$, each time in the central region. The magenta and the cyan hatched regions display the regions enclosed by the upper and lower quartiles of the corresponding fractions in the mocks for the low- and high-redshift bin, respectively. The blue line displays the fraction for 2dGRS-2PIGG groups in the redshift range $0.03 \leq z \leq 0.13$, and the blue shaded region is the uncertainty given by $\pm 0.2$ error in the absolute magnitude estimation of the 2dGRS galaxies.

White 2007), which reproduce the complex selection function of the actual spectroscopic survey. During the extensive testing and comparing of these groupfinders, we have developed a new method that progressively optimizes the group-finding parameters for smaller and smaller groups as the catalog is generated from the richest groups down to the poorest. This is found to optimize the group catalog fidelity, in terms of completeness and purity, over a broad range of richnesses $N$. Using this new approach, we achieve an impressively high fidelity of our group catalog compared with others in the literature at these redshifts. The standard FOF algorithm yields a group catalog with overall better statistics compared with those of the VDM algorithm, and we have chosen this for basic group catalog. However, the purity of the group sample is significantly enhanced, at modest cost in completeness, if we also take the intersection of this FOF main catalog with an independent VDM group catalog—producing the so-called “one-way-matched” (1WM) subcatalog.

With the aid of our mocks, we have a very good idea of the statistical properties of the group sample. We find that for FOF groups with $N \geq 5$ the completeness is 85% and the purity 78%. For the 1WM catalog, the purity rises to 82%, while the completeness drops only to 81%. For poorer groups with $N < 5$ the statistics of purity and completeness are not substantially worse. These fidelity statistics are fairly stable over the whole redshift range. As would be expected, the completeness and “interloper fraction” statistics for group members are enhanced in the centers of groups. Furthermore, we find that, while the basic FOF catalog slightly overproduces the number of groups with $N \leq 5$, the 1WM subcatalog reproduces almost perfectly the number of real groups down to $N = 2$.

The actual zCOSMOS 10 k FOF group catalog contains 102 groups with $N \geq 5$ and 23 groups with $N \geq 8$. Going down to $N = 2$ yields a total of 800 groups. Groups with $N \geq 5$ have been assigned a velocity dispersion $\sigma$ and a mock calibrated dynamical mass $M$ whose uncertainties are understood quite well. While for $N < 5$ we could still assign a meaningful mass to the groups, a reasonable estimate of velocity dispersion is not possible. The fraction of 10 k galaxies in groups is about 25% at low redshift and decreases toward $\sim 15\%$ at $z \sim 0.8$.

Comparing the 10 k group catalog to the mocks yields fairly consistent results. The main discrepancies are that (1) there are many more groups with $N \geq 20$ in the mocks compared to the 10 k sample, and (2) the fraction of 10 k galaxies in groups is significantly higher at $z \sim 0.9$ than in the mocks. We find that the fraction of galaxies in groups, for groups with a given corrected richness $N_{\text{corr}} (\geq 20)$, decreases from redshift 0.1 to redshift 0.8. This can be interpreted in terms of growth of structure as expected in a hierarchical structure formation scenario.

The properties of these groups are explored in a number of companion papers. The environments of these groups in terms of the larger scale galaxy-density-field in which they are embedded is given in Kovač et al. (2009). The evolution of the galaxy population in these groups is explored in A. Iovino et al. (2009, in preparation) and K. Kovač et al. (2009, in preparation), in terms of galaxy colors and galaxy morphologies respectively, and in Silverman et al. (2009) in the context of active galactic nuclei. In future studies, we will investigate the X-ray properties of our groups, and perform a weak lensing and a galaxy-group cross-correlation analysis.

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