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Deformation Measurement of Highway Bridge Head Based on Mobile TLS Data

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ABSTRACT The precise leveling method is often used to monitor the uneven deformation of the highway bridge head, which requires manual contact, dangerous and heavy workload. In order to solve these issues, this paper proposes a method to extract deformation features of the highway bridge head based on mobile terrestrial laser scanning (TLS) point clouds. Firstly, an automatic data acquisition system is designed to analyze and determine the scanning station spacing and scanning resolution. Then acquired road point clouds are denoised based on the plane fitting method, which usually sets the experimental threshold. The road dividing line information is used for point clouds coarse registration, and the weighted average elevation method is used for refined registration. Lastly, the elevation of the deformation monitoring point is the average elevation of all points in the selected grid surface, which will mitigate random errors in the elevation of a single point. Point clouds of three different roads were collected to verify the proposed method. The results show that the accuracy of the elevation repeatability is better than ±1mm, and the accuracy of the elevation check with the TM50 total station is better than ±2mm, which meets the requirements of deformation monitoring. In addition, it takes about 3-4 minutes to complete the data collection of a station on the highway bridge head. Therefore, the proposed method based on mobile TLS data can be suitable for highway bridge head deformation measurement.

INDEX TERMS Terrestrial laser scanning (TLS), highway bridge head, deformation monitoring, automatic data acquiring system, point cloud processing.

I. INTRODUCTION

The highway bridge head is prone to uneven settlement during long-term use, and it is easy to bump when the vehicle passes at high speed, which seriously affects the safety of driving. Therefore, it is necessary to regularly monitor the uneven settlement of the highway bridge head. At present, the precise leveling method is usually used to monitor the settlement, which has high accuracy. However, when using this method, operators are required to work in the emergency lane and the personal safety of the operators cannot be effectively guaranteed [1], [2].

Obtaining a more complete model of the road, terrestrial laser scanning (TLS) overcomes the limitation of traditional surveying technologies, which measures only a few feature points. Furthermore, owing to the characteristic of non-contact measurement and high spatial resolution in a minimal amount of time-consuming, the application of TLS in the deformation monitoring of the highway bridge head will have significant technical advantages [3]–[6].

However, affected by the field environment, the obtained road point clouds have inevitable outliers. Therefore, one of the most important tasks is to eliminate outliers. Many scholars have done in-depth research in this area. Zhang et al. [7] propose an ellipse fitting algorithm based on the minimum P-norm of the residuals, and introduce an adaptive threshold to denoise the tunnel point cloud. Experimental results show that the algorithm has better robustness. Lipman et al. [8], Fleishman et al. [9], Dey and Sun [10] propose robust MLS (RMLS), adaptive MLS (AMLS) and data dependent MLS (DDMLS) to improve the moving least squares (MLS), respectively, which have better feature...
retention while denoising. Zaman et al. [11] adopt the idea of clustering to classify the point cloud data, and then select the target subject on the clustering result to achieve point cloud denoising. However, these algorithms are usually complicated, time-consuming due to differential equations construction, polynomial fitting performing and so on. Therefore, it is necessary to investigate a more efficient denoising algorithm for point clouds of highway bridge head.

In order to unify the coordinate system of point clouds scanned from different stations, it is necessary to register the point cloud data. The conventional registration method is to set the target as a feature point for registration around the scanning field [12], but this method is limited to the operating scene, and especially not suitable for non-contact requirement of highway settlement measurement. Zhang [13] propose a registration method based on geographic scene, which adopts a three-step registration scheme of sequence stitching, global matching and data fusion, which can better meet the registration needs of special geographic scenes. Zhang et al. [14] propose a robust algorithm for point cloud registration based on the characteristics of building planes, and compare with iterative closest point (ICP) method, proving that the algorithm is effective. Zhu and Davari [15] investigate the efficiency of registration of different feature combinations for 3D architectural scenes. 31 actual scenes show that the scale-invariant feature matching method is more accurate. However, there are few obvious geographic or architectural features in highway and any two site clouds are very similar, which make the ICP registration method unsuitable for highway point cloud registration. In addition, some novel and effective algorithms for planar registration and segmentation have been proposed recently [16]–[18], such as unsupervised robust planar segmentation, procedural shape priors-based building facades segmentation and a multiscale tensor voting method. Especially, Wu et al. [18] improve the selection of seed points in region-growing algorithm and obtain comprehensive planar segmentation results, which are more robust than clustering-based methods. Yet, the uneven deformation monitoring of the highway bridge head requires lower plane accuracy, which is generally about ±2cm, and higher elevation accuracy, which is generally better than ±5mm [19]. Therefore, considering the special requirements of the highway bridge head deformation monitoring and computational loads, an improved registration method needs to be further studied.

In addition, extracting the monitoring point elevation based on the processed point clouds is an important step for deformation monitoring. Roberts and Matthew [20] use TLS point clouds to extract the deformation information of the concrete beams of the building, and check with a total station, finding that the accuracy is the same in the range of 3-35m. Zogg and Ingensand [21] conduct a viaduct load test using TLS, showing that the difference between TLS and precision level is less than 1mm, indicating that TLS can achieve millimeter-level deformation monitoring. Lõhmus et al. [22] monitor the vertical deformation of the two bridges by TLS and find that the average difference with the precision level method is about 2 mm, which can be used as a supplement to the precision level method. Most of the above researches focus on the deformation monitoring of reinforced concrete structures with regular shape, but less research on highway bridge head, whose surface features are not regular.

The paper aims to extract deformation information of highway bridge head based on mobile TLS point clouds. In Section 2, the data acquisition system and its implementation are described in detail. Then, the point cloud processing and deformation extraction are described in Section 3. The Section 4 presents three different scenarios to verify the proposed method. The conclusion is given in Section 5.
of a three-dimensional laser scanner (Z+F), a mobile carrier, a fixed frame, and an automatic leveling base. The Z+F Image 5010c is amongst the fastest 3D laser scanner in the market [23].

The scanner and the auto-leveling base are fixed on the roof of a car through a fixing frame, which can realize the real-time automatic leveling of the scanner. The data acquisition software has been developed, which will facilitate the control of the scanner in the car. The main functions of the data acquisition software include project settings, scanning parameter settings, and point clouds preview. The communication with the scanner is realized through wireless local area network (WLAN), and the corresponding IP address and port are set through the software. The project settings mainly include the scan data storage path, scanning file name, and the scanning parameter settings mainly include the scanner’s acquisition resolution, quality, and acquisition mode. At the end of the scan task, the software automatically pops up a preview interface of the point clouds. The point clouds are collected in a stop-and-go operation mode, which makes the motion carrier remain stationary every certain distance. After the current scanning is completed, the carrier moves forward according to a preset distance, and continues to get road point cloud data. The above steps are repeated until all the roads to be detected are scanned. In order to improve the data collection efficiency and ensure the accuracy of the point clouds, reasonable station spacing and scanner parameters are very important [24], [25].

B. STATION SPACING

Due to the limitation of the field of view and the ranging range, multiple stations need to be arranged on the highway for scanning separately. The larger the distance between the stations, the fewer the total number of stations required, and the shorter the scanning time. However, an excessively large distance between the stations will lead to a reduction in the quality of the point cloud data, which is caused by an excessively large incident angle of the laser on the ground. Incident angle refers to the angle between the emission direction of the laser and the normal to the surface of the scanning target. The larger the incident angle of scanning, the greater the measurement error [21]. The basic principle is shown in Figure 2.

As shown in Figure 2, the largest incident angle is located at the point S, and the geometric relationship between the station distance (2L), the scanner height (H), and the maximum incident angle (θ) can be expressed as:

$$\theta = \arctan \frac{L}{H}$$  \hspace{1cm} (1)

Lichti [26] show that when the incident angle is greater than 75°, the scanning error starts to rise sharply. According to Equation (1), when θ is less than 75°, L is less than 3.7 * H. The height of the scanner from the ground is about 2.2 m, so L ≈ 8.2 m, and the station spacing can be set to 16m.

C. SCANNER PARAMETERS

The scanner parameters mainly include scanning resolution, scanning quality, scanning initial attitude, scanning time, etc. This section focuses on analyzing the settings of scanning resolution and scanning initial attitude.

The resolution of Z + F scanner has 6 levels, including “low, middle, high, super high, ultra-high, extreme high”. The higher the resolution, the higher the density of the point cloud. The higher density reveals the clearer the details of the scanned object, however, the more time which takes to scan. Dot spacing, scan time and angular step for different resolutions of Z + F scanner are shown in Table 1.

![FIGURE 2. Geometrical relationship between the scanning system and road.](image)

As mentioned above, the optimal station spacing is 16m, that is, the maximum distance between the target point and the scanner is 8m. In addition, according to the needs of data processing, the dot spacing should be no more than 5mm. Therefore, in order to ensure the highest scanning efficiency, “Super high” resolution can be used.

Proper scanning initial attitude is conducive to data processing. To facilitate the denoising of point cloud data, the X axis of the scanner is set to be parallel to the road and point in the forward direction; the Y axis of the scanner is set to be perpendicular to the road; the Z axis, X axis and Y axis are perpendicular to each other and finally form a right-handed system. The geometric relationship between the scanning coordinate system and the road is shown in Figure 3.

III. METHODOLOGY

Because point clouds are massive and scattered, it is the key to obtain true and reliable deformation information of highway bridge head from massive and scattered point clouds. This section focuses on three key issues: point clouds denoising, point clouds registration, and deformation information extraction.
A. POINT CLOUDS DENOISING

The noises in the road point clouds collected by the three-dimensions (3D) laser scanner mainly include passing vehicles, green vegetation, street lights, and airborne noise. These noises can not only increase the number of point clouds, but also seriously affect the processing and analysis of point clouds. According to the spatial distribution of point clouds, these noises can be mainly divided into two categories: (1) drifting points: significantly away from the main body (2) mixed points: confused with the correct point clouds. The first type of noise is irrelevant to the road surface and far from the main part of the road, whereas the second type of noise is related to the road and mixed with the main point cloud of the road surface, as shown in Figure 4. The point clouds were collected from a real highway experiment, which will be described in next section.

Since the initial scanning attitude is set during data acquisition, the following formula can be used for rough noise elimination:

\[-\alpha \cdot D < X < \alpha \cdot D, \quad -L < Y < n \cdot L, \quad H - h < Z < H + h\]  

(2)

where \(X, Y, Z\) are the coordinates of the point cloud, \(D\) is the distance between two adjacent stations, \(\alpha\) is the point cloud denoising adjustment coefficient, \(L\) is the width of each lane, \(n\) is the number of driving lane, \(H\) is the height of the scanner from the ground, \(h\) is the height error of \(H\). Considering the number of single-site clouds and denoising efficiency, we can empirically take \(\alpha\) equal to 0.8. According to national code for design of road engineering [27], the lane width is 3.75 m. Taking into road construction errors, we take \(L\) as 4.0 m in this paper. In addition, because the scanning operation is usually on the emergency lane, the \(Y\) value should be greater than negative \(L\) and less than \(n\) times \(L\). The \(H\) value of the scanner is about 2 m and the height error caused by the road slope is taken as 0.2 m based on national code for design of road engineering [27]. The point clouds are roughly denoised as shown in left subplot of Figure 5. As can be seen from left subplot of Figure 5, there are still a lot of noise points in the middle of the road. Therefore, further fine denoising is needed. As the road surface is approximately an inclined surface, the plane fitting of point cloud based on random sampling consistency is adopted to obtain the plane parameters [28], which are \(a, b, c, d\). Then we can compute the vertical distance from each point to the fitting plane:

\[V_i = \frac{|ax_i + by_i + cz_i + d|}{\sqrt{a^2 + b^2 + c^2}}\]  

(3)

where \(i\) is the point, \(V_i\) is the distance of the point to the fitting plane. Then we can calculate the average value of \(V_i\) the values at all points:

\[V_{\text{mean}} = \frac{\sum_{i=1}^{n} V_i}{n}\]  

(4)

When \(V_i\) is greater than two times the \(V_{\text{mean}}\) value, this point is removed as outlier. The refined denoising point clouds are shown in right subplot of Figure 5.
B. POINT CLOUDS REGISTRATION

For the settlement monitoring of highway bridge head, the method of non-contact measurement is required. Therefore, it is not feasible to place feature points, such as target balls. In addition, the characteristics of highway bridge head point clouds are not obvious, and the clouds of any two sites are very similar, which make the ICP registration method not suitable for point clouds of highway bridge head. So, a new step-by-step registration algorithm for point clouds of highway bridge head is proposed in this section.

1) PLANAR REGISTRATION

Planar registration method utilizes conventional feature points to align [29], [30]. Supposing scanned at A station and B station, respectively, point clouds named \( P \) in the coordinate system \( O_1 - x_1y_1z_1 \) are obtained at station A, and point clouds named \( Q \) in the coordinate system \( O_2 - x_2y_2z_2 \) are obtained at station B. We adopt the common feature points of the two site clouds, such as the corner points of traffic signs, the center of the guardrail cylinder, etc. Let the feature point set of station A be \( P.T \), and that of station B be \( Q.T \). The feature point sets \( P.T (X,Y) \) and \( Q.T (x,y) \) satisfy the equation:

\[
\begin{bmatrix}
X \\
Y
\end{bmatrix} = R \begin{bmatrix}
x \\
y
\end{bmatrix} + \begin{bmatrix}
\Delta X \\
\Delta Y
\end{bmatrix}
\]

(5)

where \( R \) is the rotation matrix, \( \Delta X \) and \( \Delta Y \) are the translations in the \( X \) and \( Y \) directions. Assuming that \( \alpha \) and \( \beta \) are rotation angles, respectively, the rotation matrix can be expressed as:

\[
R = \begin{bmatrix}
cos\alpha & -sin\alpha \\
sin\alpha & cos\alpha
\end{bmatrix} \begin{bmatrix}
 cos\beta & -sin\beta \\
 sin\beta & cos\beta
\end{bmatrix}
\]

(6)

Generally, constrained by the accuracy of feature point recognition, the plane registration accuracy is about 2 cm [31], [32]. As the accuracy of monitoring the uneven settlement of the
highway bridge head is required to be within ±5 mm, this paper proposes a weighted elevation alignment algorithm based on common points for the alignment of elevation data.

2) VERTICAL WEIGHTED REGISTRATION

Due to the accurate leveling of the scanner, theoretically the cloud data height difference between the two stations is a constant. By selecting the two-site cloud public area, we can calculate the two-site cloud elevation difference.

The point clouds at station A overlapping with station B are recorded as $PA$, the distances between $PA$ and the scanning center of station B are recorded as $D_{PB}$, and the elevations of $PB$ are recorded as $H_{PB}$. The point clouds at station B overlapping with station A are recorded as $PB$, the distances between $PB$ and the scanning center of station B are recorded as $D_{PA}$, and the elevations of $PA$ are recorded as $H_{PA}$. The elevation difference between $PA$ and $PB$ is:

$$\Delta H = H_{PA} - H_{PB} \quad (7)$$

where $\Delta H$ is the elevation difference. Figure 6 shows the elevation difference sequence of the common point of station A and station B, whose point clouds are collected from the Experiment two. The two adjacent stations are Scan 2 and Scan 3.

As can be seen from Figure 6, the elevation difference between the common points of the two stations varies from $-28$ mm to $-32$ mm. This is mainly caused by the instrument shafting and leveling errors. In order to reasonably calculate

| Table 2: The operation configuration of three experiments. |

| Content          | Experiment one | Experiment two | Experiment three |
|------------------|----------------|----------------|------------------|
| Operating time   | 20-6-2019     | 20-11-2019     | 12-11-2019       |
| Operating location | Municipal road | Highway(G1501) | Highway(G10)     |
| Lane number      | 2             | 3              | 3                |
| Station Spacing  | 16 m          | 16 m           | 16 m             |
| Resolution       | Super High    | Super High     | Super High       |
| Quality Mode     | Low           | Low            | Low              |
| Scanning Range   | ~64 m         | ~70 m          | ~80 m            |
| Scanning Time    | ~15 min       | ~20 min        | ~20 min          |
| Scanning Stations| 4             | 5              | 5                |
| Round trip       | Yes           | Yes            | Yes              |

| Table 3: Statistical results of elevation differences of every adjacent stations (in mm). |

| Experiment Number | Adjacent Station | Common Points Number | Max   | Min   | Mean  | STD  |
|-------------------|------------------|----------------------|-------|-------|-------|------|
| One               | Scan1-Scan2      | 2060                 | -17   | -23   | -20   | 1.2  |
|                   | Scan2-Scan3      | 2210                 | 18    | 12    | 15    | 0.9  |
|                   | Scan3-Scan4      | 2420                 | -29   | -35   | -32   | 1.1  |
| Two               | Scan1-Scan2      | 3606                 | -26   | -33   | -29   | 0.9  |
|                   | Scan2-Scan3      | 3703                 | -27   | -33   | -30   | 0.9  |
|                   | Scan3-Scan4      | 3425                 | 23    | 17    | 20    | 1.0  |
|                   | Scan4-Scan5      | 3519                 | -19   | -25   | -22   | 1.1  |
| Three             | Scan1-Scan2      | 3980                 | 27    | 23    | 26    | 0.4  |
|                   | Scan2-Scan3      | 4500                 | 16    | 10    | 13    | 1.5  |
|                   | Scan3-Scan4      | 4626                 | -13   | -19   | -16   | 0.8  |
|                   | Scan4-Scan5      | 4870                 | -26   | -35   | -32   | 1.1  |
the elevation difference of the scanning station, a distance-based weighting method is introduced. Taking into account the distance between the common point \( i \) and scanning station, the weight of \( \Delta H_i \) can be determined as:

\[
P_i = \left( \frac{M_{PA} - D_{PA}}{M_{PA}} \right)^2 + \left( \frac{M_{PB} - D_{PB}}{M_{PB}} \right)^2
\]

where \( M_{PA}, M_{PB} \) are the maximum distances of the public point cloud from the station A to station B, \( D_{PA}, D_{PB} \) are the distances of the point \( i \) from the station A to station B. Taking the weighted average value of the elevation differences of all common points as the actual elevation difference between the two station, that is:

\[
\Delta H = \sum \frac{P_i \Delta H_i}{\sum P_i}
\]

Based on the weighted height difference between the two stations, we achieve registration in the vertical direction and eliminate the stratification phenomenon.

C. DEFORMATION INFORMATION EXTRACTION

When using traditional leveling method to monitor the highway bridge head, several leveling points are arranged in sequence only at the edge of the emergency lane, and the spacing between the leveling points is generally about 3 ~ 5 m. However, when TLS method is used, a full coverage of the road can comprehensively indicate the elevation change information of the road. In this paper, a detection point is extracted every certain distance along the longitudinal direction and transverse direction of the road. The longitudinal (road extension direction) starting point is the joint between the road and the bridge, and the transverse starting point is the edge of the emergency lane. After the plane position of the

![Experiment one: Municipal road](image)

(a) Elevation changes of two lanes in a municipal road bridge head.

![Experiment two: Highway G1501](image)

(b) Elevation changes of three lanes in G1501 highway bridge head.

![Experiment three: Highway G10](image)

(c) Elevation changes of three lanes in G10 highway bridge head.

**FIGURE 10.** Elevation changes of different lanes. Here we use the relative elevation based on a reference plan.
detection points are determined, we can calculate the elevation of each detection point. Because there is a large random error at a single point, we extract the elevation information by the average elevation of all points in the selected grid surface, as shown in Figure 7.

As shown in Figure 7, the $D$ value determines the distance between adjacent detection points, which can be determined according to actual needs. $L$ has a greater impact on the accuracy of elevation extraction. If the value of $L$ is too large, the surface selected by the square frame may be an

FIGURE 11. The chromatogram of elevation differences between the round-trip scans. The unit is mm.
inclined surface, and the elevation of the center point cannot be obtained. If the value of $L$ is too small, the number of points selected by the square frame is insufficient to prevent the effect of gross errors. Therefore, choosing a reasonable $L$ value is very important. When different $L$ values are selected, there is a difference in the elevation distribution of the points within the square frame, as shown in Figure 8.

It can be seen from Figure 8 that when $L$ is less than 0.02 m, the number of points in the area is small, and the point elevation fluctuation is small, but the distribution is irregular; when $L$ is more than 0.02 m, the number of points in the area is large, but the point elevation is fluctuating. Taking all factors into consideration, we will take $L$ as 0.02 m. Since the elevations of the points in the area basically follow the normal distribution, the average elevation value of all points is used as the elevation of the detection points.

### IV. RESULTS AND DISCUSSION

In order to verify the feasibility of the method in this paper, three experiments were conducted. The first experiment was conducted on a municipal road and was used to initially evaluate the stability of the data collection and processing. The last two experiments were conducted on two different highways and were used to assess the effectiveness of the method in the real environment. The specific details of the three experiments are shown in Table 2 and field environmental conditions are shown Figure 9. Therefore, we can calculate that the operation time of each station is about 3-4 minutes.

After collecting point clouds, the rough and refined denoising are conducted by proposed method and the result is shown in Figure 5. Considering the similarity of denoising, we only give the denoising results of Experiment two. When the denoising is completed, the planar registration is based on the corner points of the road dividing line, and then the elevation registration is based on the public point cloud. The statistical results of the elevation difference between all two adjacent stations are shown in Table 3.

It can be seen from Table 3 that there are more common points in experiment two and three than that in experiment one, which is because that the first has only 2 lanes and the last two have 3 lanes. In addition, the average standard deviation (STD) of all stations is about 1 mm, which indicates that the point cloud registration method is feasible.

Then, the deformation information acquisition method described in section 3.3 is used to extract the elevation of each lane, which are shown in Figure 10. The X axis represents the mileage of the longitudinal section of the road, and its starting point is determined according to the convenience of measurement and location of the joint between the road and the bridge. The Y axis represents the elevation change of the longitudinal section of the road. As can be seen from Figure 10, the elevation changes of different lanes on the same road are basically the same, which macroscopically shows the feasibility of extracting elevation information.

In order to verify the internal coincidence accuracy of the detection method in this paper, the same method and the same parameters were used for round-trip scanning. At the same time, four reference targets are arranged at both ends to unify the coordinate system of the round-trip data. The round-trip comparison results are shown in Figure 11. Figure 11 depicts the chromatogram of the difference between round-trip scans. The corresponding relationship between the difference and the color is plotted in the figure. It can be seen from the figure that the comparison results of the round-trip scans are overall greenish, that is, the difference is less than ±1 mm, and a light blue or light-yellow color appears in a small range, that is, the difference is greater than ±1 mm and less than ±2 mm.

In order to quantify the comparison results of the round-trip scans, according to the method in section 3.3, some points are extracted for each lane. The elevation difference of the
same detection point is compared, and the results are shown in Figure 13. It can be seen from Figure 12 that most elevation differences for three experiments are within ±1 mm, and average height differences of all lanes are basically zero, which indicates that the repeat measurement accuracy is better than ±1 mm.

To further verify the accuracy of the method in this paper, the TM50 total station was used to collect 68 measurement points in Experiment 2 and Experiment 3 respectively, which are divided into four rows along the road. At the same time, four reference targets are arranged at both ends of the road to unify the coordinate system. According to the plane coordinates of the total station detection points, the same position points in the point clouds are compared with the total station data, and the comparison results are shown in Table 4. It can be seen from Table 4 that the mean value of the elevation difference of the four rows is less than ±1 mm, and the average is −0.2 mm; the maximum standard deviation is 1.68 mm, and the average standard deviation is 1.31 mm, which indicates that the external accuracy of proposed method is better than ±2 mm.

### TABLE 4. Statistics of elevation differences between TLS method and Total station method (in mm).

| Row Number | Mean  | STD  |
|------------|-------|------|
| Experiment two |       |      |
| Row 1      | 0.07  | 1.20 |
| Row 2      | -0.30 | 1.11 |
| Row 3      | -0.24 | 1.38 |
| Row 4      | -0.59 | 1.68 |
| Experiment three |     |      |
| Row 1      | -0.42 | 1.32 |
| Row 2      | 0.18  | 1.02 |
| Row 3      | 0.35  | 1.28 |
| Row 4      | -0.47 | 1.46 |

(4) Through three different experiments, it finds that the accuracy of round-trip measurement is better than ±1 mm, and compared with the total station measurement, the external check accuracy is better than ±2 mm, which meet the requirements of highway approach deformation monitoring.

### ABBREVIATIONS

The following abbreviations are used in this manuscript:

- TLS Terrestrial laser scanning
- MLS Moving least squares
- RMLS Robust moving least squares
- AMLS Adaptive moving least squares
- DDMLS Data dependent moving least squares
- ICP Iterative closest point
- WLAN Wireless local area network
- 3D Three dimensions
- STD Standard deviation

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