Metallization of shock-compressed liquid ammonia

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Ammonia is predicted to be one of the major components in the depths of the ice giant planets Uranus and Neptune. Their dynamics, evolution, and interior structure are insufficiently understood and models rely imperatively on data for equation of state and transport properties. Despite its great significance, the experimentally accessed region of the ammonia phase diagram today is still very limited in pressure and temperature. Here we push the probed regime to unprecedented conditions, up to ∼350 GPa and ∼40 000 K. Along the Hugoniot, the temperature measured as a function of pressure shows a subtle change in slope at ∼7000 K and ∼90 GPa, in agreement with ab initio simulations we have performed. This feature coincides with the gradual transition from a molecular liquid to a plasma state. Additionally, we performed reflectivity measurements, providing the first experimental evidence of electronic conduction in high-pressure ammonia. Shock reflectance continuously rises with pressure above 50 GPa and reaches saturation values above 120 GPa. Corresponding electrical conductivity values are up to one order of magnitude higher than in water in the 100 GPa regime, with possible significant contributions of the predicted ammonia-rich layers to the generation of magnetic dynamos in ice giant interiors.

As an archetypal hydrogen-bonded system, the properties of ammonia (NH$_3$) at high pressures (P) and temperatures (T) are of particular interest in solid state physics and chemistry [1, 3]. For temperatures up to 10 000 K and pressures up to 500 GPa, theoretical studies predict an exceptionally rich phase diagram, including fluid phases of different chemical composition, solid and superionic phases [4, 6]. Unveiling these extremely intriguing behaviours has also crucial impact on planetary science because NH$_3$ has a significant cosmic abundance. As a part of the so called “planetary ice” (mixtures of water, ammonia, and methane), it is believed to be found in a wide range of thermodynamic conditions in planets and their satellites [7, 10], both within our Solar System and beyond [11, 13]. Adiabatic interior models of Uranus and Neptune predict that planetary ice exists between 20 to 600 GPa and 2000 to 7000 K [7, 14, 18], which possibly coincides with the stability range for superionic ammonia. Recent models [19, 21] more consistent with Uranus’ low luminosity observations predict much warmer interiors, with temperatures up to 25 000 K, where ammonia would rather be a warm dense ionized fluid [1, 6, 22, 23]. These non-adiabatic models highly rely on transport properties of the planetary ice at such high temperatures, which are mostly unavailable to date. Moreover, the discovery of hot Neptune exoplanets, like Gliese 436b, further extends the necessity of exploring a wide range of thermodynamic conditions [24]. Accurate determination of the high-pressure ammonia equation of state is hence required to build more reliable interior models accounting for planetary ice as a complex mixture [17, 19, 25] and overcoming the often used, yet too simplistic, approach that considers planetary ice as made of pure water. Similarly, the NH$_3$ transport properties, such as electrical conductivity, are crucial to address Uranus’ and Neptune’s peculiar magnetic fields [26, 28]. Despite its importance, experimental studies of the high pressure behavior of ammonia remain very scarce and limited to a narrow thermodynamic range. Measurements in diamond anvil cells have characterized the equation of state and phase diagram up to 200 GPa at 300 K, but reached at most ∼40 GPa at higher temperatures (∼3000 K) [29, 30]. Few studies have been carried out employing dynamic compression methods, mainly at gasgun facilities, providing shock compression data up to 70 GPa [37, 42]. However, no reflectivity data were obtained, only two temperature points were reported [40] and only two electrical conductivity data points exceeded 40 GPa [41]. The dearth in experimental data is undoubtedly linked to the severe difficulties in preparing appropriate samples for high pressure experiments, in particular those using laser-driven shocks.

In this work, we report on the first laser-generated shock compression experiment in ammonia, which allowed us to study the equation of state and optical reflectivity (tightly linked to electronic conductivity) in an unprecedented regime, up to ∼ 350 GPa and 40 000 K, together with new ab initio calculations. The experiment was performed at the LULI2000 laser facility at the LULI Laboratory in France. The setup is
shown schematically in Fig. 1a. A long pulse (τ_L ~ 1.5-5 ns) high-energy (E_L up to 1 kJ at λ_L = 527 nm) laser beam was focused (~500 μm smoothed focal spot) on the target to generate a compression shock wave. In order to reach relevant pressures, we have conceived and assembled a specific target capable to accommodate liquid ammonia and compatible with standard laser-shock experiments. Gaseous NH₃ was first condensed at low temperatures (~243 K) in a small stainless steel cell-target. Two thin α-quartz windows of 50 μm and 250 μm were used at the front (laser-side) and back (diagnostic side) of the cell respectively, to ensure tightness and allow optical probing. A CH-Al pusher was glued on the outer part of the front side SiO₂ window to avoid any contamination of the sample. The system was then brought to ambient temperature, allowing an outgoing controlled flow to maintain an almost constant pressure and avoid breaking of the thin quartz windows under the thermal pressure increase. Finally, the initial Hugoniot state was fixed at 14 bar, room temperature (~295 K), and a density of 0.61 g/cm³ (based on NIST database). The Raman spectrum of the filled cell is consistent with that of pure liquid ammonia without any measurable impurities (see Fig. 1b). Visible diagnostics were used to probe shocked ammonia. A dual-channel velocity interferometer system for any reflector (VISAR) 43 44 operated at 532 nm and 1064 nm (sensitivities of 4.96 km/s and 12.81 km/s) was used to measure the time-dependent shock velocity for equation of state measurements and reflectivity. The shock-front reflectivity at 532 nm was also measured independently with a reflectometer. A streaked optical pyrometer (SOP) 45 47 collected the self-emission of the shocked sample as a function of time to gather temperature estimation. Typical experimental data are shown in Fig. 1c/d. Quartz (front side window) and ammonia are both rapidly ionized and transformed into a reflecting state upon shock compression. The instantaneous shock velocity in both materials could therefore be measured with the VISARs, knowing the values of the quartz and ammonia pristine refractive indices (n₀Q and n₀NH₃ respectively) (see Supplementary Material). Using quartz as in situ standard and applying impedance mismatch 48 49 together with the Rankine-Hugoniot relations 50 we get the thermodynamic conditions (mass density ϱ, pressure P and internal energy E) in shocked ammonia at the SiO₂/NH₃ interface 51.

In addition to the experiment, we performed ab initio simulations using density functional theory molecular dynamics (DFT-MD) using VASP 52 55. The Hugoniot states were calculated based on previous ab initio EOS data 6 derived with the Perdew-Burke-Ernzerhof (PBE) exchange-correlation functional 56. Here, we extended these calculations and calculated reflectivity and DC electrical conductivity with both the PBE and the HSE 57 58 hybrid functional 59.

FIG. 1. a. Schematic experimental setup of the laser pulse inducing shock compression in the liquid ammonia sample. b. Raman spectrum of the sample indicative of pure liquid NH₃ with ν₁-ν₃ stretching band around 3300 cm⁻¹ as well as ν₂ and ν₄ modes (inset) at 1200 cm⁻¹ and 1600 cm⁻¹, respectively. c. VISAR signal and d. SOP data together with the extracted velocity and temperature measurements. For this shot, laser energy and pulse length were respectively 816 J and 2 ns.

FIG. 2. Hydrodynamic conditions probed in shocked liquid ammonia (ρ₀ = 0.61 g/cm³). a. Relation between shock and particle velocities. Also shown are previous measurements at an initial density of 0.69 g/cm³ 57 58 50 and the previous (dashed lines) and present (continuous lines) DFT-MD data considering both initial states. b. Corresponding pressure–density diagram.

The experimental data for the Hugoniot are presented
Temperature is one of the most difficult parameters to access and up to now only two experimental data points were available at \( \sim 4000 \text{ K} \) \[40\]. Our data set, shown in Fig. 3, provides a much wider ensemble up to very high temperatures. The consistency with calculations is remarkable, except for the highest points where the experimental uncertainties are larger. In particular, in both calculations and experiment we find that the shock temperature increases continuously up to \( \sim 7000 \text{ K} \) (\( \sim 90 \text{ GPa} \)), where a slight change of slope occurs, see Fig. 3.

In solids this kind of behavior is often linked to phase transitions, including melting (ex. \[61\], \[62\]). To understand the origin of this feature in ammonia, we have computed the site-site pair correlation functions along the Hugoniot, shown in Fig. 4. The analysis of these calculations indicates that the observed change in slope in the \( P-T \) curve is caused by dissociation processes in the molecular liquid and its transformation into a plasma state. In the N-H pair correlation function in Fig. 4, the drop of the intramolecular bond peak at 1.08 Å with increasing temperature illustrates the gradual dissociation of the ammonia molecules. We also observe additional peaks in the H-H and N-N pair correlation functions above 2000 K, which are indicative of the formation of \( \text{H}_2 \) and \( \text{N}_2 \) molecules. Even more complex and very short-lived molecules such as \( \text{N}_2\text{H}_3 \) and \( \text{HN}_3 \) were observed from visual inspections of the ionic trajectories in the DFT-MD. It can be seen that the characteristic \( \text{H}_2 \) signal in Fig. 4 vanishes above 5000 K and that the broad feature corresponding to different forms of N-N bonding (between 1.0 Å and 1.5 Å in Fig. 4) reaches its maximum at 7000 K–8000 K. This implies that the molecular \( \text{NH}_3 \) liquid transforms through continuous dissociation and ionization processes into a plasma. Additionally, diffusion coefficients and vibrational spectra confirm that \( \text{NH}_3 \) molecules dissociate between 6000 K and 8000 K (see Supplementary Material). This behaviour reveals that along the Hugoniot the chemistry in ammonia is richer in small molecular species compared to water, which dissociates into simple ionic and atomic species at similar shock pressures \[63\].

In Fig. 5, shows the measured reflectivities at 532 nm and 1064 nm, together with the DFT-MD calculated values, using either the PBE \[56\] or HSE \[57, 58\] exchange-correlation functionals. Included are also predictions from Ref. \[22\]. Our data suggest a gradual rise in shock reflectivity with pressure, with a smooth transition from a low- to a highly-reflecting state between \( \sim 50 \) GPa and \( \sim 120 \) GPa.

Present calculations are in good agreement with the experimental data. In particular, they match the saturation values at both wavelengths remarkably well. We find a relatively small influence of the exchange-correlation functional, due to partial compensation of errors that occurs in the Fresnel formula between the indexes of refraction for the initial \( (n_0) \) and final \( (n) \) Hugoniot states (see the Supplementary Material). Note that the HSE calculations reproduce the initial index of refraction \( (n_0^{HSE} = 1.34) \) much better than the PBE calculations \( (n_0^{PBE} = 1.42) \) if compared to the experimental value \( (n_0^{exp} = 1.32) \). The disagreement between our DFT-MD results and previous calculations is mainly explained by an incorrect setting of \( n_0 = 1 \) by Li et al. \[22\], which leads to a shifted onset of reflectivity increase and significantly too high saturation values in their data.
Reflectivity is closely related to DC electrical conductivity $\sigma(\omega = 0)$, which is a crucial quantity for, e.g., plasma diagnostics and planetary dynamo models. Our \textit{ab initio} calculations show that the frequency behavior of $\sigma(\omega)$ is very different from a Drude behavior (see Supplementary Material), which is often assumed to derive DC conductivities from optical reflectivities [64–67]. The calculated DC electronic conductivity is regarded as highly reliable considering the excellent agreement between \textit{ab initio} and experimental reflectivity data. It rises systematically with Hugoniot pressure (Fig. 5b). The lowest DC conductivity point at $\sim$ 21 GPa and 2000 K is in good agreement with previous experiments [38, 60]. Interestingly, we find significantly higher values than those measured in Ref. [41] between 50 GPa and 75 GPa and calculated in Li \textit{et al.} [22]. A possible explanation for this deviation may be the higher initial density of $\varrho = 0.69$ g/cm$^3$ compared to our Hugoniot, so that results from Refs. [22, 61] between 50 GPa and 75 GPa might describe a different phase, most likely the superionic phase [6]. Above 75 GPa, the values calculated by Li \textit{et al.} [22] agree reasonably well with our results. We also note that overall the NH$_3$ conductivity is larger than the one of water along the Hugoniot. Even when the ionic contribution is added for water [63], the ammonia conductivity remains one order of magnitude higher in the 100 GPa regime, due to the different dissociation mechanisms, as discussed above.

In conclusion, we report novel equation of state measurements of warm dense ammonia in a previously unachieved regime, together with the first experimental evidence of ammonia metallization we observed in

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**FIG. 4.** a. H-H, b. N-H, and c. N-N pair correlation functions for different temperatures along the Hugoniot (solid lines). The dashed lines indicate bond lengths in various molecules that were visually observed in the simulations.

**FIG. 5.** a. Reflectivity at 532 nm (green) and 1064 nm (orange) versus pressure. Small orange and green dots correspond to time-resolved experimental reflectivities measured in 11 decaying shots. Thick orange and green lines are Hill fits to the experimental data with the reflectivity imposed to be zero at $U_s = 0$ km/s. Diamonds and square correspond to the DFT reflectivities computed in this study respectively with the PBE and HSE functionals. Large dots show DFT reflectivities from Ref. [22]. b. Calculated DC electrical conductivity of NH$_3$ along the Hugoniot (black squares) compared to previous DFT-MD results [22] and experimental data [38, 11, 60]. The electronic and total electrical conductivity along the principal H$_2$O Hugoniot are also shown as gray filled and empty squares, respectively [63].
the reflectivity. These high quality data on such an experimentally challenging compound provide a unique benchmark for our ab initio calculations. The simulations indicate a complex dissociation mechanism in ammonia, comprising three regimes: a molecular fluid, in which NH₃ molecules still persist, a complex fluid above 20 GPa, in which NH₃ molecules start to dissociate and N₂ and N₃ bounded molecules are formed, and a completely dissociated plasma state above 90 GPa. The electrical conductivity is surprisingly high and one order of magnitude higher than that of water at ~100 GPa. This finding is particularly useful to revisit dynamo models of Uranus and Neptune magnetic fields, as the only existing conductivity data at lower pressures suggest the opposite trend.[29] Models that entirely disregarded ammonia in the past should now consider the possible contribution of the predicted ammonia-rich layers[29] to have better insights of the dynamo process in ice giant planets. Future work should extend our study to the superionic domain to estimate the extent and the physical properties of the potential superionic layers within ice giant planets.

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