Spectroscopy and frequency measurement of the $^{87}\text{Sr}$ clock transition by laser linewidth transfer using an optical frequency comb

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We performed spectroscopic observations of the 698-nm clock transition in $^{87}\text{Sr}$ confined in an optical lattice using a laser linewidth transfer technique. A narrow-linewidth laser interrogating the clock transition was prepared by transferring the linewidth of a master laser (1064 nm) to that of a slave laser (698 nm) with a high-speed controllable fiber-based frequency comb. The Fourier-limited spectrum was then observed for an 80-ms interrogating pulse. We determined that the absolute frequency of the $5s^2 \ 1S_0 – 5s5p \ 3P_0$ clock transition in $^{87}\text{Sr}$ is 429 228 004 229 872.0 (1.6) Hz referenced to the SI second. © 2014 The Japan Society of Applied Physics

The precise measurement of time and frequency is of great interest for a wide range of applications, including fundamental science and metrology. Optical frequency standards have been extensively studied, and great strides have been made in improving their frequency stability and reducing uncertainty over the past few decades. Optical clocks have been realized with various ions and atoms including $\text{Al}^+$, $\text{Hg}^+$, $\text{Sr}^+$, and $\text{Yb}$. Because some optical clocks have already outperformed the best microwave clocks, they are being studied by the International Committee for Weights and Measures (CIPM) with a view to rede

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Figure 1 shows a schematic diagram of our experimental setup. The master laser was a monolithic nonplanar-ring-oscillator (NPRO) Nd:YAG laser emitting at 1064 nm with a free-running linewidth of several kilohertz. The frequency of the master laser was stabilized to a high-finesse ULE cavity by using the Pound–Drever–Hall method. The instantaneous linewidth of the master laser was less than 3.5 Hz. However, the linewidth including frequency jitter at an averaging time of several seconds was 10 Hz. We compensated for the linear frequency drift of the master laser (85 Hz/s) caused by the creep of the reference cavity by using an acousto-optic modulator (AOM). A fiber comb equipped with an intracavity EOM was used to obtain a broad servo bandwidth for linewidth transfer. The repetition rate of the comb was approximately 43.4 MHz. The carrier-envelope offset frequency was detected by using a conventional f–2f interferometer and stabilized to a hydrogen maser at our institute. Our fiber-based frequency comb is described in detail elsewhere. A heterodyne beat between the master laser at around 1064 nm and the comb component (\( f_{\text{comb-YAG}} \)) was detected to stabilize the repetition rate of the comb by using the intracavity EOM. The linewidth of the comb components was reduced to the hertz level owing to the broad servo bandwidth (approximately 1.4 MHz) of the EOM. The clock laser was a homemade extended cavity diode laser (ECDL) with an antireflection-coated diode laser. The free-running linewidth of the ECDL was \( \approx 300 \) kHz. The ECDL generated 20 mW of output light with an injection current of 70 mA. A heterodyne beat note was observed by mixing part of the ECDL output (1 mW) and the second-harmonic comb modes around 698 nm, which were generated by a periodically poled lithium niobate (PPLN) crystal. The ECDL was phase-locked to one appropriate mode of the narrow-linewidth optical comb by employing direct feedback control to the injection current of the diode laser. The servo bandwidth of the phase-locking was approximately 700 kHz. The tight phase lock allowed the linewidth of the comb to be transferred to the ECDL. The remaining output of the ECDL traveled through a double-pass AOM to control the laser frequency and was used for the spectroscopy of the \( ^1S_0 \rightarrow ^3P_0 \) transition. The narrow-linewidth comb was also used for preparing the narrow-linewidth cooling laser for the intercombination MOT at 689 nm (not shown in Fig. 1). The Sr optical lattice clock operates with lattice-confined \(^{87}\)Sr atoms with nuclear spin I = 9/2. After two-stage laser cooling using the \( ^1S_0 \rightarrow ^3P_1 \) transitions and the \( ^1S_0 \rightarrow ^3P_1 \) transitions, about \( 10^5 \) atoms were loaded onto a vertically oriented one-dimensional (1D) optical lattice. The lattice laser was generated by an ECDL at 813 nm and amplified by a tapered amplifier (TA). A transmission grating was used to remove the amplified spontaneous emission generated by the TA. The polarization axis of the lattice laser was parallel to that of the clock laser and an applied magnetic field during optical pumping and spectroscopy. The lattice laser frequency was set at 368 554.72(6) GHz, where we confirmed experimentally that the differential AC Stark shift of the clock transition was canceled. The lattice laser frequency was stabilized to another frequency comb and monitored with a wavemeter. The trap depth of the lattice was \( 24E_r \) (where the recoil energy \( E_r = k_B = 170 \) nK). The clock laser was injected from the retroreflection mirror of the optical lattice and aligned coaxially with the lattice laser so that the clock laser was coupled to the fiber of the lattice laser. The beam diameter of the clock laser was \( \approx 310 \) μm, which was much larger than that of the lattice beam (180 μm). The larger beam waist ensured the homogeneous excitation of the atoms. To reduce line-pulling and collision shifts, the atoms were optically pumped to either of the stretched states \( |m_F = \pm 9/2 \rangle \) by a circularly polarized 25-ms light pulse resonant with the \( ^1S_0 \rightarrow ^3P_1 \) (\( F = 9/2 \) transition). During optical pumping, a homogeneous magnetic field of 91 μT parallel to the polarization of the lattice and clock lasers was used to define the quantization axis. The magnetic field was maintained during the spectroscopy. To observe the clock transition, a first \( \pi \) pulse by the clock laser...
was applied to the stretched-state atoms $|m_F = \pm 9/2\rangle$ in the optical lattice to excite the atoms from the $^1S_0$ state to the $^3P_0$ state. To count the number of unexcited atoms, we measured the fluorescence ($I_{\text{unexcited}}$) on the strong $^1S_0 - ^3P_1$ transition using an electron multiplying charged coupled device (EM-CCD) camera. We then applied a second $\pi$ pulse of 4.5 ms to repump the atoms in the $^3P_0$ state to the $^1S_0$ state and counted the number of excited atoms by measuring the fluorescence ($I_{\text{excited}}$). Figure 2 shows a typical Zeeman component ($m_F = -9/2$) signal $[I_{\text{excited}} / (I_{\text{excited}} + I_{\text{unexcited}})]$ obtained by the first $\pi$ pulse of 80 ms. A lineshape of 10 Hz is observed with a high excitation probability. The spectral structure of the $m_F = \pm 7/2$ component resulting from the imperfect optical pumping was not observed. Therefore we neglected the line-pulling effect in the frequency measurement. For the clock operation, we optically pumped the atoms to each of the stretched states in turn. The interrogation cycle for each stretched state was 2 s. By averaging the frequency of the two states, we could eliminate the first-order Zeeman shift and determine the line center of the clock transition. In practice, by probing both sides of the spectrum at its full width at half maximum, the deviation of the clock laser frequency from the atomic resonance could be detected and used to stabilize the clock laser frequency.

For absolute frequency measurements, the repetition rate of the frequency comb used for the linewidth transfer and the frequency driving the AOM to stabilize the clock laser were recorded by frequency counters, whose microwave references were coordinated universal time UTC(NMIJ). Figure 3(a) shows six absolute frequency measurements obtained over five days (May 23 to 27, 2013). Figure 3(b) shows a typical Allan standard deviation of the measured absolute frequency [measurement $\pm 3$ in Fig. 3(a)] against UTC(NMIJ). The Allan standard deviation was $2.4 \times 10^{-13}$ for an 8-s averaging time, and it improved after a 3700-s averaging time to $2.0 \times 10^{-15}$. We note that the measured Allan deviation follows the stability of UTC(NMIJ). The uncertainty was given by the Allan standard deviation at the longest averaging time for each measurement [e.g., the uncertainty for measurement $\pm 3$ in Fig. 3(a)] was calculated by using the Allan standard deviation in Fig. 3(b)]. The standard deviation of the measurements of over five days [shown in Fig. 3 (a)] was calculated to be $9.3 \times 10^{-16}$, which indicates the measurement statistics in the experiment.

The corrections and uncertainties for the $^{87}$Sr optical lattice clock are listed in Table I. The largest correction was due to the blackbody radiation shift, which was estimated to be $55.3(2.3) \times 10^{-16}$ for the temperature of the vacuum chamber $[T = 303(3)\text{ K}]$. For the AC Stark shift caused by the lattice laser, the second-order Zeeman shift, and the collision shift, we experimentally determined the systematic shift by employing an interleaved scheme, in which we varied the parameters to be investigated between two values synchronized with the clock cycle. The AC Stark shift caused by the lattice laser, second-order Zeeman shift, and collision shift were determined experimentally to be $0.0(1.8) \times 10^{-16}$, $-4.3(1.1) \times 10^{-16}$, and $0.0(2.1) \times 10^{-16}$, respectively. The AC Stark shift induced by the clock laser was estimated to be $-0.2(2) \times 10^{-16}$. The gravitational shift was calculated to be $22.7(6) \times 10^{-16}$ by using the height of the trapped atoms from the geoid surface of 20.9(5) m. While stabilizing the clock laser to the clock transition, we recorded the excitation ratio and evaluated the servo error to be $0.5 \times 10^{-16}$. All the above corrections add up to $37.0 \times 10^{-16}$ with an uncertainty of $3.8 \times 10^{-16}$ (Table I).

UTC(NMIJ) is compared with International Atomic Time (TAI) via a satellite link at five-day intervals. However, because the Sr lattice clock was operated several hours a day, we conservatively estimate the uncertainty attributed to the measurement time gap to be $33.0 \times 10^{-16}$ based on the frequency variation of UTC(NMIJ). The results of the frequency link between UTC(NMIJ) and TAI can be found in Circular T, which is published on the BIPM web page.

From Circular T 305, the correction of the link between
UTC(NMIJ) and TAI was found to be $-6.9(13.1) \times 10^{-16}$. The correction between TAI and SI of $4.0(2.0) \times 10^{-16}$ was also obtained from Circular T 305.

The total systematic uncertainty of the absolute frequency measurement in Table I is $37.0 \times 10^{-16}$ (1.6 Hz), including the measurement statistics. The inclusion of the corrections in Table I gives a final absolute frequency of $429 228 004 229 872.0 (1.6)$ Hz referenced to the SI second. Figure 4 shows the frequencies of the $^{87}$Sr clock transition measured at different laboratories. Our measurement result agrees with measurements performed at different laboratories within the uncertainty. The measured absolute frequency will be reported to the CIPM via the next Consultative Committee for Time and Frequency meeting scheduled for 2015 and will contribute to discussions regarding updating of the recommended frequency value of the $^{87}$Sr lattice clock, which is one of the secondary representations of the second.

**Fig. 4.** Comparison of the absolute frequencies of the $^{87}$Sr clock transition measured at different laboratories. The horizontal solid and broken lines represent the recommended value and its uncertainty for $^{87}$Sr by the CIPM in 2013. The solid circles represent the data used for the 2013 CIPM recommendation. The red solid rectangle represents the result of this work.

**Table 1.** Frequency corrections and their uncertainties.

| Effect                          | Correction ($10^{-16}$) | Uncertainty ($10^{-16}$) |
|---------------------------------|-------------------------|--------------------------|
| Blackbody radiation             | 55.3                    | 2.3                      |
| AC Stark (lattice)              | 0.0                     | 1.8                      |
| AC Stark (probe)                | 0.2                     | 0.2                      |
| Second-order Zeeman             | 4.3                     | 1.1                      |
| Collision                       | 0.0                     | 2.1                      |
| Gravitation                     | $-22.7$                 | 0.6                      |
| Servo error                     | 0.0                     | 0.5                      |
| Sr systems total                | 37.0                    | 3.8                      |
| UTC(NMIJ)                       | —                       | $33.0^{9}$               |
| UTC(NMIJ)–TAI                   | $-6.9$                  | 13.1                     |
| TAI–SI                          | 4.0                     | 2.0                      |
| Measurement statistics          |                         | 9.3                      |
| Total                           | 34.1                    | 37.0                     |

a) The uncertainty is due to the short measurement time. See text.

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