Short-range repulsion and isospin dependence in the $K\bar{N}$ system

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Abstract

The short-range properties of the $K\bar{N}$ interaction are studied within the meson-exchange model of the Jülich group. Specifically, dynamical explanations for the phenomenological short-range repulsion, required in this model for achieving agreement with the empirical $K\bar{N}$ data, are explored. Evidence is found that contributions from the exchange of a heavy scalar-isovector meson ($a_0(980)$) as well as from genuine quark-gluon exchange processes are needed. Taking both mechanisms into account a satisfactory description of the $K\bar{N}$ phase shifts can be obtained without resorting to phenomenological pieces.

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I. INTRODUCTION

The kaon-nucleon ($KN$) system provides an ideal setting for studying short-distance effects of the hadron-hadron force. This is because pions play a much less important role in the $KN$ system than in the most extensively studied nucleon-nucleon ($NN$) system. Indeed, the one-pion-exchange is absent in the $KN$ interaction and the contributions from $2\pi$-exchange to the interaction seem to be weaker than in the $NN$ system. Under such circumstances one expects that short-distance effects can be most easily isolated from the attractive medium-range background and that possibly effects from explicit quark-gluon degrees of freedom can be identified.

A large body of work accumulated in the last 50 years indicates that meson degrees of freedom are very efficient for describing low-energy hadron-hadron interactions. In particular for the $KN$ system, a few years ago the Jülich group presented a meson-exchange model for the $K^+N$ scattering [1,2]. Ref. [1] considered single boson exchanges ($\sigma$, $\rho$, $\omega$), together with contributions from higher-order diagrams involving $N$, $\Delta$, $K$ and $K^*$ intermediate states. It turned out that the $S$-wave observables of $KN$ experiments could only be described with the model if the value of the $KK\omega$ coupling constant is increased about 60% above the value that follows from the SU(3) (quark flavor) symmetry. Specifically, the increased value of the $KK\omega$ coupling constant was strictly necessary to obtain the $S$-wave low-energy parameters and the energy dependence of $S$-wave phase shifts for both isospin $I = 0$ and $I = 1$ channels. However, this increased value lead to additional repulsion in the $P$ and higher partial waves which seemed to be not favored by the empirical data, especially in the $P_{03}$ and $P_{13}$ channels. Thus, it was concluded in Ref. [1] that the required additional contributions must be much shorter ranged than the $\omega$ exchange.

Further evidence for the conjecture that the repulsion needed to describe $KN$ scattering cannot be interpreted completely in terms of conventional $\omega$-exchange came from subsequent investigations of the $\bar{K}N$ system [3]. In a meson-exchange model like the one developed by the Jülich group there is a close connection between the $KN$ and $\bar{K}N$ interactions due to G-parity conservation. Specifically, this means that the repulsive $\omega$-exchange changes sign for $K^-N$, because of the negative G-parity of the $\omega$-meson, and becomes attractive. A large contribution from the $\omega$-exchange as favored by the $KN$ $S$-waves turns then into a strongly attractive piece – which is indeed much too strong to fit the $K^-N$ data [3].

The conclusion from those results was that $\omega$-exchange, as treated in this model, can only be interpreted as an effective contribution that parameterizes besides the “physical” $\omega$-exchange also further shorter-ranged mesonic contributions or genuine quark-gluon effects or both. This was shown by a model analysis where the coupling constants of the $\omega$ meson ($g_{KK\omega}, g_{NN\omega}$) were kept at their SU(3) symmetry values and an additional phenomenological (extremely short-ranged) repulsive contribution, a “$\sigma_{rep}$”, with a mass of about 1.2 GeV was added - see Figs. 1(a) and 1(b).

In Ref. [2] the model was further refined by replacing $\sigma$– and $\rho$–exchange by the correlated $2\pi$–exchange contribution in the $J^P = 0^+$ and $J^P = 1^-$ channels, respectively, as illustrated

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1The spectroscopic notation used is such that a partial wave with angular momentum $L$, total angular momentum $J$ and isospin $I$ is denoted by $L_{I,J}$. 
in Fig. 1(c). This was done by starting from a microscopic model for the $t$–channel reaction $N\overline{N} \rightarrow K\overline{K}$ with $\pi\pi$ (and $K\overline{K}$) intermediate states and using a dispersion relation over the unitarity cut. Such a realistic model of (effective) $\sigma$– and $\rho$–exchange was then used to reconstruct an extended meson exchange model for $K\overline{N}$ scattering. But again, as is Ref. [1], the addition of a phenomenological $\sigma_{\text{rep}}$ was essential to describe the data with the SU(3) $KK\omega$ coupling constant.

One possible interpretation for the need of a very short-ranged repulsion, shorter ranged than that provided by $\omega$-exchange, is that quark-gluon effects are playing a role [1]. The study of the $KN$ interaction in the context of quark models has a long history since the 1980’s [4]. More recently, the subject has gained renewed interest with the works of Barnes and Swanson [5] and Silvestre-Brac and collaborators [6–8]. The main ingredients in the calculations of both groups are the nonrelativistic quark model and a quark interchange mechanism with one-gluon-exchange (OGE). One important conclusion of these calculations is that the derived $KN$ interaction is short-ranged and repulsive, and strongly isospin dependent. As we discussed above, although in the Jülich model the overall strength and energy dependence of the $S$-wave phase-shift of $K^+N$ scattering can be obtained by augmenting the value of the $KK\omega$ coupling, the $P$ and higher partial waves do not come out right and the introduction of the exchange of a fictitious scalar particle with repulsive character was essential for this matter. In view of this, the substitution of an isospin independent $\sigma_{\text{rep}}$ by a strongly isospin-dependent quark-gluon dynamics is not trivial and apparently bound to fail. However, we note that in both Refs. [1,2] the $a_0(980)$ meson was left out without apparent reason. This meson, being a scalar-isovector, is an important source of isospin dependence and it has a mass not much larger than those of the other mesons considered in the model. Thus, it can, in principle, play an important role for the isospin dependence of the $KN$ interaction.

The main motivation of our paper is to investigate the energy and isospin dependences of the $KN$ interaction in a hybrid model, in which the Jülich model is extended by adding the $a_0(980)$ exchange, and where the very short-ranged part of the $KN$ interaction is described by quark-gluon exchange, instead of the phenomenological $\sigma_{\text{rep}}$. We construct an effective $KN$ potential from a microscopic nonrelativistic quark model from the interquark exchange mechanism and use all components of the OGE interaction. These include the Coulomb, spin-independent contact and spin-orbit interactions. In addition, we use a linearly rising potential to represent quark confinement.

The paper is organized as follows. In the next section we describe the $KN$ meson-exchange model of the Jülich group. In section III we provide an overview of studies on the $KN$ system that were carried out in the framework of the quark-model. In section IV we present and discuss our results. Specifically, we investigate the consequences of replacing the phenomenological $\sigma_{\text{rep}}$ of the Jülich model by quark-gluon exchange. Our conclusions and perspectives are presented in Section V. Appendix A presents the expressions for the effective $KN$ potentials in the quark model.

II. THE JÜLICH $KN$ MODEL

The Jülich meson-exchange model of the $KN$ interaction has been widely described in the literature [1,2,9,10] and we refer the reader to those works for details. Here we will only
summarize the features which are relevant for the present study.

The Jülich meson-exchange model of the $KN$ interaction was constructed along the lines of the (full) Bonn $NN$ model [11] and its extension to the hyperon-nucleon ($YN$) system [12]. Specifically, this means that one has used the same scheme (time-ordered perturbation theory), the same type of processes, and vertex parameters (coupling constants, cut-off masses of the vertex form-factors) fixed already by the study of these other reactions.

The diagrams considered for the $KN$ interaction are shown in Fig. 1. Based on these diagrams a $KN$ potential $V$ is derived, and the corresponding reaction amplitude $T$ is then obtained by solving a Lippmann-Schwinger type equation defined by time-ordered perturbation theory:

$$ T = V + VG_0T. $$

From this amplitude phase shifts and observables (cross sections, polarizations) can be obtained in the usual way.

As seen in Fig. 1, obviously the Jülich model contains not only single-meson (and baryon) exchanges, but also higher-order box diagrams involving $NK^*$, $∆K$ and $∆K^*$ intermediate states. Most vertex parameters involving the nucleon and the $\Delta(1232)$ isobar can be taken over from the (full) Bonn $NN$ potential. The coupling constants at vertices involving strange baryons are fixed from the $YN$ model (model B of Ref. [12]). Those quantities $(g_{NΛK}, g_{NΣK}, g_{NY^*K})$ have been related to the empirical $NNπ$ coupling by the assumption of SU(6) symmetry, cf. Ref. [1,2].

For the vertices involving mesons only, most coupling constants have been fixed by SU(3) relating them to the empirical $ρ \rightarrow 2π$ decay. Exceptions are the coupling constants $g_{KKσ}$ and $g_{KKω}$, which have been adjusted to the $KN$ data, for the following reason: The $σ$ meson (with a mass of about 600 MeV) is not considered as a genuine particle but as a simple parametrization of correlated $2π$-exchange processes in the scalar-isoscalar channel. Therefore, its coupling strength cannot be taken from symmetry relations. Concerning the $ω$-exchange it was found that a much larger strength than obtained from SU(3) was required in order to obtain sufficient short-range repulsion for a reasonable description of the $S$-wave $KN$ phase shifts [1]. The $ω$-coupling $g_{KKω}$ had to be increased by about 60% over the symmetry value - quite analogous to the situation in the $NN$ system [11]. However, such an increased $ω$-exchange turned out to be in contradiction with the empirical data on $P$- and higher partial waves. Specifically $P_{03}$ and $P_{13}$ do not really demand additional repulsive contributions. Thus, it was concluded that the additional repulsion should be of rather short-ranged nature. Such a contribution would still allow to obtain a reasonable description of the $S$-waves, but would leave $P$- and higher partial waves basically unchanged.

As a consequence the Jülich group presented a model where the coupling strengths for both $g_{NNω}$ and $g_{KKω}$ were kept at their SU(6) values. At the same time a phenomenological, very short-ranged contribution was added. This phenomenological piece has the same analytical form as $σ$-exchange, but an exchange mass of 1200 MeV and, most importantly, an opposite sign. Accordingly, it was denoted $σ_{rep}$.

In a subsequent investigation the $σ(600)$ and also the elementary $ρ$ were replaced by a microscopic model for correlated $2π$ (and $K\bar{K}$) exchange between kaon and nucleon, in the corresponding scalar-isoscalar and vector-isovector channels [2]. Starting point for this was a model for the reaction $N\bar{N} \rightarrow K\bar{K}$ with intermediate $2π$ and $K\bar{K}$ states, based
on a transition in terms of baryon \((N, \Delta, \Lambda, \Sigma)\) exchange and a realistic coupled channel \(\pi \pi \rightarrow \pi \pi, \pi \pi \rightarrow K \bar{K},\) and \(K \bar{K} \rightarrow K \bar{K}\) amplitude. The contribution in the \(s\)-channel is then obtained by performing a dispersion relation over the unitarity cut. But also in this model the phenomenological short-ranged \(\sigma_{\text{rep}}\) was needed in order to achieve agreement with the empirical phase shifts.

Since the results of Ref. [2] indicate that the contributions of the correlated \(2\pi\) exchange in the scalar-isoscalar channel are in rough agreement with the effective description by \(\sigma\)-exchange used in Ref. [1] we will employ the latter in the present investigation for simplicity reasons. Specifically, we will use the \(KN\) model I presented in Ref. [2]. The parameters of this model are summarized in Table I. Resulting phase shifts for the Jülich model I [2] will be shown and compared with empirical data in sect. IV. Further results, including also scattering observables can be found in Ref. [2].

III. THE \(KN\) INTERACTION IN THE QUARK MODEL

In this section we briefly review the salient features of model calculations of the \(KN\) interaction that are based on quark-gluon exchange and derived within the nonrelativistic quark model. Specifically, we will focus on the more recent calculations of Barnes and Swanson [5] and Silvestre-Brac and collaborators [6–8].

Barnes and Swanson use the quark-Born-diagram (QBD) method [13]. In this method, the \(KN\) scattering amplitude is assumed to be the coherent sum of all one-gluon-exchange (OGE) interactions followed by all allowed quark line exchanges. The input to this method is the microscopic quark-quark interaction and kaon and nucleon wave functions. Barnes and Swanson [5] used the contact spin-spin “color-hyperfine” component of the OGE and used Gaussian wave functions for the interacting hadrons, which allowed them to evaluate the \(KN\) scattering amplitude analytically. They calculated isospin \(I = 0\) and \(I = 1\) scattering observables such as \(S\)-wave phase shifts and scattering lengths. The model has only two parameters, the ratio of the \(u,d\) to \(s\) quark masses, \(\rho = m_q/m_s\), and \(\alpha_s/m_q^2\), where \(\alpha_s\) is the quark-gluon coupling constant. By using typical quark-model parameters and using the Born approximation, Barnes and Swanson obtained very reasonable results for the \(S\)-wave phase shifts [5].

The studies of Silvestre-Brack and collaborators [6–8] complement the work of Barnes and Swanson in several aspects. First of all, Refs. [6–8] employ the RGM instead of the QBD method. The main difference between the two methods refers to the way orthogonality effects in the relative \(KN\) wave functions are treated. These are effects due to the Pauli principle for quarks in different clusters. It can be shown [14] that the differences between effective hadron-hadron interactions calculated with both methods are usually small, although not entirely negligible. In Ref. [6] the authors calculate \(S\)-wave scattering phase shifts using the Coulomb, spin-spin and constant contact pieces of the OGE quark-quark interaction. In addition, they include the exchange of \(\pi\) and \(\sigma\) mesons - considered as elementary particles - between quarks, and a linearly rising confining potential. The same quark-quark interaction is used to build the \(K\) and \(N\) wave functions and to generate the \(KN\) interaction. The parameters are constrained to reproduce the low-lying meson and baryon spectrum. The main conclusion of this study was that it is impossible to describe both \(I = 0\) and \(I = 1\) isospin channels simultaneously within the model. Relativistic kinetic energy effects were
investigated Ref. [7]. The results obtained for the $S$-waves, for which one expects such effects to be more important, were not much different from the corresponding nonrelativistic ones. In Ref. [8], scattering phase shifts from $S$- up to $G$-waves were calculated. The difference from Ref. [6] is that a spin-orbit interaction was added to the OGE and confining pieces used there. No meson exchanges between quarks were considered. The parameters were again fixed by requiring a good description of the low-lying meson and baryon spectrum. The results obtained are such that the $I = 0$ $S$-wave phase shift is reasonably well described, while the corresponding $I = 1$ is too repulsive. The $P$ and higher partial-wave phase shifts are poorly described, with the exception of the $P_{11}$, $D_{13}$, $D_{15}$, and $G_{19}$ phases. The $P_{01}$ phase, for example, is predicted to be almost zero, while the corresponding experimental phase grows from zero up to 60 degrees at $p_{lab} = 1$ GeV.

The results of Silvestre-Brac and collaborators [6–8] clearly indicate that the quark-interchange mechanism with OGE alone is not sufficient to describe the $K^+ N$ data. However, it seems to provide at least enough strength for $S$-waves. In view of the discussion above on the Jülich model, we investigate here the substitution of $\sigma_{rep}$ in that model by the quark-interchange mechanism with OGE. Recently, one of us [15] has derived the contribution of the spin-spin part of the OGE to the central part of the $K N$ interaction using the mapping formalism developed in Ref. [14]. The different contributions to the $K^+ N$ effective potential from the quark-interchange mechanism are illustrated in Fig. 2. The on-shell $K N$ amplitude is identical to the one derived by Barnes and Swanson [5]. In order to iterate the potential in a Lippmann-Schwinger equation one needs the off-shell amplitude. For this purpose, we have calculated the contributions of all remaining components of the OGE to the $K^+ N$ effective potential within the framework of Ref. [14]. We found that the spin-spin component of the OGE gives by far the most important contribution to the $K^+ N$ effective potential.

For illustrative purposes we present, in this section, the phases calculated in Born approximation - in the next section the OGE $K N$ potential is iterated in the Lippmann-Schwinger type of equation, Eq. (1). In Fig. 3 we present the $S$- and $P$-wave phase shifts resulting from the OGE and the confining interaction. The higher partial waves are very small and are not shown. The experimental data points in this figure are taken from Refs. [16–18]. The analytical expressions for the $K N$ potential are given in the Appendix. The parameters of the potential are the masses of the constituent quarks, $m_q (= m_u = m_d)$ and $m_s$, the quark-gluon hyperfine coupling $\alpha_s$, and the size parameters of the nucleon and kaon wave functions, $\alpha$ and $\beta$. We use the “reference parameter set” of Barnes and Swanson [5], which are conventional quark model parameters. These are

\begin{align}
\rho &= m_q/m_s = 0.33 \text{ GeV}/0.55 \text{ GeV} = 0.6 \\
\alpha_s/m_q^2 &= 0.6/(0.33)^2 \text{ GeV}^2 \\
\alpha &= 0.4 \text{ GeV} \\
\beta &= 0.35 \text{ GeV}.
\end{align}

The string tension of the confining potential is taken to be $\sigma = 0.18 \text{ GeV}^2$ [19]. In addition, when calculating the phase shifts we use the physical masses of the nucleon and the kaon, $M_N = 0.940$ GeV and $M_K = 0.495$ GeV. Fig. 3 shows that $S$-waves are reasonably well described by the model, although the $I = 0$ phase agrees less well with the data at higher energies. The fit can be improved slightly by choosing another set of parameters, as done by Barnes and Swanson in their study of the $S$-wave phase shifts [5]. In this paper we maintain
the reference set, since the general trend of the higher partial waves will not be modified by a change of the quark model parameters.

In Fig. 4 we show the separate contributions of the OGE and confining interaction to $S$ and $P$ phases. The dominance of the spin-spin component of OGE is clearly seen. The confining interaction gives a very small contribution to all waves, and the only noticeable effect from the other components of the OGE is the one from the Coulomb part in the $S_{11}$ wave.

IV. RESULTS AND DISCUSSION

As discussed in the last two sections, the $KN$ interaction in the low-energy region ($p_{lab} \leq 1$ GeV/c) can be well understood within the meson-exchange picture. However, a good quantitative overall description of the data can only be achieved by adding a phenomenological contribution that is extremely short-ranged and repulsive - and therefore affects essentially the S-waves only. At the same time interaction models based on quark-gluon degrees of freedom yield only a mediocre overall reproduction of the $KN$ phase shifts. However, the predicted S-waves are in fairly good agreement with empirical results suggesting that at least the short-ranged part of the $KN$ interaction is well accounted for by the one-gluon exchange mechanism that is the dominant ingredient in those quark models. It is therefore tempting to combine the contributions of those two complementary approaches to the $KN$ force. Indeed such a procedure is in the spirit of the original $KN$ model of the Jülich group where it was suggested that the short-ranged phenomenological piece added in this model might be an effective parametrization of either further short-ranged mesonic contributions or of genuine quark-gluon effects or both [1,20].

Results for the $KN$ phase shifts of the original Jülich model (note that we use here model I of Ref. [2]) are shown by the dash-dotted lines in Fig. 5. If we switch off the contribution from the phenomenological $\sigma_{rep}$ and add the contribution from one-gluon exchange instead we obtain the short dashed lines. The parameters of the quark model are the same as in the previous section. We see that the OGE is indeed capable of producing repulsive contributions which are of a comparable order of magnitude as the one of the phenomenological $\sigma_{rep}$. Indeed, after the discussion in sect. III this could have been expected. However, it is definitely surprising that for the $S_{11}$ partial wave the results with OGE (and without $\sigma_{rep}$) are almost identical to the ones of the original Jülich model. In case of the $S_{01}$ the situation is somewhat less satisfying. Here the repulsion provided by the OGE is significantly smaller than the one parametrized by the $\sigma_{rep}$. This is simply a consequence of the isospin dependence inherent in the OGE – the phenomenological $\sigma_{rep}$ is, of course, per construction an isoscalar. The higher partial waves (in the $I = 0$ as well as the $I = 1$) are again only marginally changed as compared to the original results - testifying that also the OGE is of rather short range.

The above results can be seen as an indication that the OGE is not the only short-range physics that is parametrized by the $\sigma_{rep}$ of the Jülich $KN$ model. (Indeed one might argue that this could have been already guessed from the difference in the isospin structure!) Besides possible higher-order contributions resulting from quark-gluon dynamics one should not forget to take into consideration also further shorter-ranged mesonic contributions. Indeed the exchange of the $a_0(980)$ meson, which is a scalar-isovector particle, is a
natural candidate for this. With its mass of about 1 GeV its contributions are definitely of short-ranged nature as required. Furthermore, its isospin structure leads to attractive contributions in the $I = 1$ channel but to repulsive contributions in the $I = 0$ channel. Thus, it complements the isospin dependence of the OGE in an almost ideal way and in conjunction with the latter would lead to contributions that are almost isospin independent – as those of the phenomenological $\sigma_{rep}$. The $a_0(980)$ meson is taken into account in the Bonn $NN$ model [11] (it is denoted as $\delta$ meson there). However, for unexplained reasons, it was not included in the original Jülich $KN$ model. Subsequent investigations of the Jülich group on the structure of the $a_0(980)$ meson suggested that this resonance can be understood in terms of strong correlations in the $\pi\eta - K\bar{K}$ channel [21]. Thus, the situation is similar to the strong $\pi\pi - K\bar{K}$ correlations in the scalar-isoscalar channel that are usually effectively parametrized by the $\sigma$ meson. Accordingly, it is in the spirit of the Bonn/Jülich models of hadronic reactions to consider the contributions of the $a_0(980)$ meson, and indeed it is included in the more recently developed models of the $\pi N$ [22,23] and hyperon-nucleon ($YN$) [24] interactions. Following the arguments in Refs. [21,22] we do not view the $a_0$ exchange as a genuine meson exchange but rather as a parametrization of correlations in the mesonic systems in the scalar-isovector channel. Therefore we consider the $a_0$ coupling constants as free parameters. In principle, $g_{K\bar{K}a_0}$ could be determined from the $a_0$ decay width into the $K\bar{K}$ system. However, the experimental information on this quantity is still very poor, cf. Ref. [25], and thus cannot provide more than a guideline. Note that in the $a_0$ exchange the product of the $NNa_0$ and $K\bar{K}a_0$ coupling constants appear, and therefore we also list only this product in Table I.

Results including now $a_0$ meson-exchange as well as the OGE contributions are shown by the long-dashed lines in Fig. 5. The coupling strength of the $a_0$ exchange has been chosen in such a way that the model prediction for the $S_{01}$ partial wave agrees roughly with the result of the original Jülich $KN$ model. As can be seen in Fig. 5, the inclusion of the $a_0$ exchange influences also the $KN P$-waves in the $I = 0$ channel, i.e. the $P_{01}$ and $P_{03}$, whereas all other higher partial waves remain basically unchanged. As a matter of fact, the present model based on $a_0$ meson exchange and OGE contributions yields pretty much the same results as the original Jülich model utilizing the phenomenological $\sigma_{rep}$. Minor differences occur only in the $S_{11}$ partial wave, which turns out to be now somewhat too less repulsive in comparison to the data. Thus, as a last step, we have slightly re-adjusted the parameters of the $\sigma$ meson, cf. Table I, which then leads to the final results shown by the solid lines in Fig. 5. Those results provide clear evidence that a comparable quantitative description of the $KN$ interaction can be achieved with a model that avoids phenomenological contributions like the $\sigma_{rep}$ of the original Jülich model.

Finally, we want to address the question whether a description of the $KN$ interaction is possible within the Jülich model without introducing explicit contributions from the OGE. Treating the coupling constants of the $\sigma$ and $a_0$ mesons as completely free parameters we were indeed able to obtain a reasonable reproduction of the $S_{01}$ and $S_{11}$ partial waves. However, it could only be achieved by assuming that the $\sigma$-exchange contribution is basically zero. Of course, this is completely unrealistic in view of the results obtained for the strength of the correlated two-pion exchange in the $\sigma$ channel in Ref. [2]. Moreover, the description of the higher partial waves deteriorates significantly if the $\sigma$-exchange contribution is so strongly reduced.
V. CONCLUSIONS AND PERSPECTIVES

In this paper we have studied the short-range properties of the $KN$ interaction. In particular, we have taken the $KN$ meson-exchange model of the Jülich group and we explored possible dynamical explanations for a phenomenological (extremely short-ranged) repulsive contribution, a “$\sigma_{\text{rep}}$” with a mass of about 1.2 GeV, that is present in the Jülich model. Such a phenomenological, repulsive and rather short-ranged piece had to be introduced in that model for achieving agreement with the empirical $KN$ data.

The very short-ranged nature of this repulsion could be a sign that quark-gluon dynamics is playing a role. Therefore, we have calculated corresponding contributions to the $KN$ interaction based on the nonrelativistic quark model and a quark interchange mechanism with one-gluon-exchange. It turned out that those processes are indeed short-ranged and repulsive. However, unlike the phenomenological “$\sigma_{\text{rep}}$” in the Jülich model, they are also strongly isospin dependent. Thus, one-gluon-exchange alone can certainly not explain the required short-range physics. Consequently, we examined additional short-range physics that arises in the mesonic sector, and specifically the exchange of the (scalar-isovector) $a_0(980)$ meson. Its contribution was not included in the original Jülich $KN$ model.

Due to its isospin structure the $a_0(980)$ exchange provides attraction in the $I = 1$ channel and repulsion in the $I = 0$ channel, and therefore counterbalances the isospin dependence of the one-gluon exchange. Taking both mechanisms ($a_0$- as well as one-gluon exchange) into account yields a short-ranged and repulsive but basically isospin-independent interaction – similar to the one parametrized by the $\sigma_{\text{rep}}$ – and, consequently, a satisfactory description of the $KN$ phase shifts can be obtained without resorting to phenomenological pieces, as demonstrated in the present paper.

The authors of the original Jülich $KN$ model conjectured that the introduced phenomenological $\sigma_{\text{rep}}$ might be an effective parametrization of either further short-ranged mesonic contributions or genuine quark-gluon effects or both [1]. Our investigation provides strong evidence that the third alternative is realized. Specifically, it lends support to the supposition that effects from quark-gluon degrees of freedom can be explicitly seen in the $KN$ system. Still one can raise the question whether contributions from genuine quark-gluon dynamics are really needed. E.g., couldn’t their role be taken over by the exchange of heavier vector mesons, say? To answer this question it will be very instructive to study the $\bar{K}N$ system again, using the present model. For example, the investigations in Ref. [3] have shown that the $\bar{K}N$ data require only a strongly reduced short-ranged repulsive piece, i.e. only about 20% of the phenomenological $\sigma_{\text{rep}}$ used in the $KN$ system. It will be interesting to see whether the present scenario of combined $a_0(980)$ exchange and quark-gluon dynamics is able to generate these properties when going over to the $\bar{K}N$ system. One should note, however, that the treatment of the $\bar{K}N$ channel in the nonrelativistic quark model is more complicated than the $KN$ system since it involves $s$-channel gluon exchange. Special care must be taken with such processes because it is not clear that the use of perturbative massless gluons makes physical sense in this model. Contributions of intermediate hybrid $q\bar{q}g$ states to the process must certainly be considered. Still the extension of the quark interchange model to incorporate gluon annihilation in the $\bar{K}N$ system would be a very interesting new development. Investigations along this line are planned for the future.
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APPENDIX A: CONTRIBUTIONS TO THE KN INTERACTION FROM OGE AND CONFINEMENT

In this Appendix we present the different contributions of the OGE and of the confining potential to the KN potential used in the present paper. Let’s denote the initial and final three-momenta of the interacting quarks by \( \vec{k}_1, \vec{k}_2, \vec{k}'_1 \) and \( \vec{k}'_2 \) (prime means final state). It is convenient to define the following combinations of momenta 
\[
\vec{q} = \vec{k}'_1 - \vec{k}_1 = \vec{k}_2 - \vec{k}'_2,
\]
\[
p_1 = (\vec{k}_1 + \vec{k}'_1)/2 \quad \text{and} \quad p_2 = (\vec{k}_2 + \vec{k}'_2)/2.
\]
In terms of these, the interquark interaction can be written as
\[
H_{OGE} = \sum_{ij} \left[ \sum_a F^a(i) F^a(j) \right] V_{ij}(\vec{q}, \vec{p}_i, \vec{p}_j), \tag{A1}
\]
where \( i, j \) identify the quarks (or antiquarks) 1, 2 and \( V_{ij}(\vec{q}, \vec{p}_i, \vec{p}_j) \) depends on spin variables and the indicated momenta. The color SU(3) matrices \( F^a(i) \), \( a = 1, \cdots 8 \), are given in terms of the Gell-Mann matrices \( \lambda^a \) as
\[
F^a(i) = \lambda^a/2 \quad \text{when} \quad i \text{ is a quark} \quad \text{and} \quad F^a(i) = -\lambda^a T/2 \quad \text{when} \quad i \text{ is an antiquark} \quad (T \text{ means transpose}).
\]
We refer the reader to the literature for the explicit expression of \( V_{ij}(\vec{q}, \vec{p}_i, \vec{p}_j) \) - see for example, Eq. (3) of Ref. [19].

Next, we present the individual contributions in \( V_{ij}(\vec{q}, \vec{p}_i, \vec{p}_j) \) to the KN potential. We represent each contribution to the KN potential as
\[
V(\vec{p}, \vec{p}') = \frac{1}{2} \sum_{D=a}^d \left[ V_D(\vec{p}, \vec{p}') + V_D(\vec{p}', \vec{p}) \right], \tag{A2}
\]
where \( \vec{p} \) and \( \vec{p}' \) are the initial and final c.m. momenta of the the KN system, and the index \( D \) identifies the diagrams \( a, \cdots d \) of Fig. 2. The explicit evaluation of these diagrams requires also the specification of the nucleon and kaon wave functions, \( \Psi_N \) and \( \Psi_K \). These are taken to be in momentum space of the form
\[
\Psi_N(\vec{p}) = \delta(\vec{p} - \vec{k}_1 - \vec{k}_2 - \vec{k}_3) N(\vec{p}) \phi(\vec{k}_1) \phi(\vec{k}_2) \phi(\vec{k}_3), \tag{A3}
\]
where
\[
\phi(\vec{k}) = \left( \frac{1}{\pi \alpha^2} \right)^{3/4} \exp \left( -\vec{k}^2/2\alpha^2 \right) \quad \text{and} \quad N(\vec{p}) = \left( 3\pi \alpha^2 \right)^{3/4} \exp \left( \vec{p}^2/6\alpha^2 \right), \tag{A4}
\]
and
\[
\Psi_K(\vec{p}) = \delta(\vec{p} - \vec{k}_q - \vec{k}_\bar{q}) \left( \frac{1}{\pi \beta^2} \right)^{3/4} \exp \left[ -\frac{(m_1 \vec{k}_q - m_2 \vec{k}_\bar{q})^2}{8 \beta^2} \right], \tag{A5}
\]
with
\[ m_1 = \frac{2m_q}{m_q + m_{\bar{q}}} \quad m_2 = \frac{2m_{\bar{q}}}{m_q + m_{\bar{q}}}. \] (A6)

For convenience we also introduce the quantities
\[ \rho = m_q/m_s \quad g^2 = \alpha/\beta \quad b = 1/\alpha. \] (A7)

The explicit contributions of the different pieces of the OGE and of the confining potential to the effective \( K N \) interaction are given by the following expressions.

1. **Coulomb**

\[ V_{D}^{\text{Coul}}(\vec{p}, \vec{p}') = 4\pi\alpha_s \omega_D(I) \int_0^\infty ds \eta_D(s) \exp \left[ -A_D(s)p^2 - B_D(s)p'^2 + C_D(s)\vec{p} \cdot \vec{p}' \right], \] (A8)

where the variable \( s \) comes in because we have chosen to perform a Laplace transform of the Coulomb potential \( 1/q^2 \) in order to integrate over the variable \( q \), and the coefficients \( \omega_D(I) \) (\( I \) identifies isospin \( I = 1 \) or \( I = 0 \)) come from summing over color-spin-flavor of quarks. The functions \( A_D, B_D, C_D, \) and \( \eta_D \) for each diagram can be written as a ratio \( A_D = n(A_D)/d(A_D), \ldots, \eta_D = n(\eta_D)/d(\eta_D) \).

**Diagram (a):**

\[ n(A_a) = 24 b^4 \beta^2 + 9 b^2 m_1^2 + (80 b^2 \beta^2 + 24 b^4 \beta^4 - 48 b^2 \beta^2 m_1 + 6 m_1^2 + 18 b^2 \beta^2 m_1^2) s \]
\[ n(B_a) = n(A_a) \]
\[ n(C_a) = 8 b^4 \beta^2 + 3 b^2 m_1^2 + (-16 b^2 \beta^2 + 8 b^4 \beta^4 + 16 b^2 \beta^2 m_1 + 2 m_1^2) s \]
\[ n(\eta_a) = 3 \sqrt{3} b^3/8 \pi^3 \]
\[ d(A_a) = d(B_a) = 6 d(C_a) = 48 \beta^2 [3 b^2 + (2 + 3 b^2 \beta^2) s] \]
\[ d(\eta_a) = [3 b^2 + (2 + 3 b^2 \beta^2) s]^{3/2} \]
\[ \omega_a(1) = -4/9 \quad \omega_a(0) = 0. \] (A9)

**Diagram (b):**

\[ n(A_b) = -24 - 80 b^2 \beta^2 + 24 b^4 \beta^4 + 12 m_1 + 60 b^2 \beta^2 m_1 - 9 b^2 \beta^2 m_1^2 \]
\[ - (96 \beta^2 + 176 b^2 \beta^4 - 48 b^4 \beta^6 - 48 \beta^2 m_1 - 6 \beta^2 m_1^2 + 120 b^2 \beta^4 m_1 - 18 b^2 \beta^4 m_1^2) s \]
\[ n(B_b) = 12 + 20 b^2 \beta^2 - 24 b^4 \beta^4 - 6 m_1 - 18 b^2 \beta^2 m_1 \]
\[ + (48 \beta^2 + 8 b^2 \beta^4 - 48 b^4 \beta^6 - 24 \beta^2 m_1 - 12 b^2 \beta^4 m_1 - 3 \beta^2 m_1^2 - 9 b^2 \beta^4 m_1^2) s \]
\[ n(C_b) = 2 b^4 \beta^2 + 2 b^2 (m_1 - 1) + (4 b^4 \beta^4 - 8 b^2 \beta^2 + 8 b^2 \beta^2 m_1 + m_1^2) s \]
\[ d(A_b) = 2 d(B_b) = 12 \beta^2 d(C_b) = 24 \beta^2 [1 + 3 b^2 \beta^2 + (4 \beta^2 + 6 b^2 \beta^4) s] \]
\[ \omega_b(1) = 4/9 \quad \omega_b(0) = 0 \] (A10)

**Diagram (c):**
\[ A_c(s) = 64 b^4 \beta^2 + 12 b^6 \beta^4 - 60 b^1 \beta^2 m_1 + 21 b^2 m_1^2 + 36 b^4 \beta^2 m_1^2 \]
\[ + (320 b^2 \beta^2 + 96 b^4 \beta^4 - 192 b^2 \beta^2 m_1 + 24 m_1^2 + 72 b^2 \beta^2 m_1^2) s \]
\[ B_c(s) = 256 b^4 \beta^2 + 12 b^6 \beta^4 - 132 b^4 \beta^2 m_1 + 21 b^2 m_1^2 + 36 b^4 \beta^2 m_1^2 \]
\[ + (320 b^2 \beta^2 + 96 b^4 \beta^4 - 192 b^2 \beta^2 m_1 + 24 m_1^2 + 72 b^2 \beta^2 m_1^2) s \]
\[ C_c(s) = -32 b^4 \beta^2 + 4 b^6 \beta^4 + 32 b^4 \beta^2 m_1 + 7 b^2 m_1^2 \]
\[ + [32 b^4 \beta^4 + 64 b^2 \beta^2 (m_1 - 1) + 8 m_1^2] s \]
\[ \eta_c(s) = 24 \sqrt{3} b^3 / \pi^3 \]
\[ d(A_c) = d(A_b) = 6 d(A_c) = 48 \beta^2 [7 b^2 + 6 b^4 \beta^2 + (8 + 12 b^2 \beta^2) s] \]
\[ d(\eta_c) = [7 b^2 + 6 b^4 \beta^2 + (8 + 12 b^2 \beta^2) s]^{3/2} \]
\[ \omega_c(1) = 4/9 \quad \omega_c(0) = 0 \quad \text{(A11)} \]

Diagram (d):

\[ n(A_d) = 80 b^2 + 160 b^4 \beta^2 + 12 b^6 \beta^4 - 72 b^2 m_1 - 132 b^4 \beta^2 m_1 + 21 b^2 m_1^2 + 36 b^4 \beta^2 m_1^2 \]
\[ + (320 b^2 \beta^2 + 96 b^4 \beta^4 - 192 b^2 \beta^2 m_1 + 24 m_1^2 + 72 b^2 \beta^2 m_1^2) s \]
\[ n(B_d) = n(A_d) \]
\[ n(C_d) = -16 b^2 - 32 b^4 \beta^2 + 4 b^6 \beta^4 + 8 b^2 m_1 + 20 b^4 \beta^2 m_1 + b^2 m_1^2 \]
\[ + (64 b^2 \beta^2 + 32 b^4 \beta^4 + 64 b^2 \beta^2 m_1 + 8 m_1^2) s \]
\[ n(\eta_d) = -24 \sqrt{3} b^3 / \pi^3 \]
\[ d(A_d) = d(B_d) = 6 d(C_d) = 48 (2 + 3 b^2 \beta^2) (1 + 2 b^2 \beta^2 + 4 b_2^2 s) \]
\[ d(\eta_d) = [(2 + 3 b^2 \beta^2) (1 + 2 b^2 \beta^2 + 4 b_2^2 s)]^{3/2} \]
\[ \omega_d(1) = -4/9 \quad \omega_d(0) = 0 \quad \text{(A12)} \]

2. Spin-orbit

\[ V_D^{SO}(\vec{p}, \vec{p}') = i(\vec{p} \times \vec{p}') \cdot \vec{S}_N w_D^{SO}(\vec{p}, \vec{p'}), \quad \text{(A13)} \]

with \( S_N \) the spin operator of the nucleon and

\[ w_D^{SO}(\vec{p}, \vec{p}') = 4 \pi \alpha_s \omega_D(I) \int_0^\infty ds \eta_D(s) \exp \left[-A_D(s) p^2 - B_D(s) p' t^2 + C_D(s) \vec{p} \cdot \vec{p}' \right], \quad \text{(A14)} \]

where the functions \( A, B, C \) are the same as in the Coulomb potential, and the \( \eta_D \)'s are given by

\[ \eta_a(s) = \frac{3 \sqrt{3} b^5 (8 - 3 m_1)}{32 \pi^3 [3 b^2 + (2 + 3 b^2 \beta^2)] s^{5/2}} \]
\[ \eta_b(s) = -\frac{3}{8 \pi^3} \sqrt{3} \frac{b^3 \beta^3 (m_1 - 2) (4 b^2 \beta^2 + m_1)}{2 [1 + 3 b^2 \beta^2 + (4 b^2 + 6 b^2 \beta^2)] s^{5/2}} \]
\[ \eta_c(s) = -\frac{3\sqrt{3}b^5 \left( m_1 - 4 - 2b^2\beta^2 \right)}{\pi^3 \left( 7b^2 + 6b^4\beta^2 + (8 + 12b^2\beta^2) s \right)^{5/2}} \]

\[ \eta_d^{(1)}(s) = -\frac{3\sqrt{3}b^4 \beta^4 (1 + 2b^2\beta^2) (2b^2\beta^2 + m_1) (28b^4\beta^4 + m_1^2 + 8b^2\beta^2 + 8b^2\beta^2 m_1)}{2\pi^3 (2 + 3b^2\beta^2)^{3/2} (1 + 4b^2\beta^2 + 3b^4\beta^4) (4 + 2b^2\beta^2 - m_1) [1 + 2\beta^2 (b^2 + 2s)]^{5/2}} \]

\[ \eta_d^{(2)}(s) = \frac{3\sqrt{3}b^3 \beta^3 (2b^2\beta^2 + m_1) (28b^4\beta^4 + m_1^2 + 8b^2\beta^2 + 8b^2\beta^2 m_1)}{2\pi^3 (2 + 3b^2\beta^2)^{5/2} (4b^2\beta^2 + m_1) [1 + 2\beta^2 (b^2 + 2s)]^{5/2}} \]

\[ \omega_a(0) = -\frac{4}{3} \frac{1}{m^2}, \quad \omega_a(1) = +\frac{8}{9} \frac{1}{m^2} \]

\[ \omega_b(0) = +\frac{2}{9} \left( \frac{1}{m^2} - \frac{1}{m_s^2} \right), \quad \omega_b(1) = -\frac{4}{27} \left( \frac{1}{m^2} - \frac{1}{m_s^2} \right) \]

\[ \omega_c(0) = +\frac{1}{3} \frac{1}{m^2}, \quad \omega_c(1) = -\frac{1}{9} \frac{1}{m^2} \]

\[ \omega_d^{(1)}(0) = -\frac{1}{9} \left( \frac{1}{m^2} + \frac{4}{mm_s^2} \right), \quad \omega_d^{(1)}(1) = -\frac{1}{27} \left( \frac{1}{m^2} + \frac{8}{mm_s^2} \right) \quad (A15) \]

\[ \omega_d^{(2)}(0) = +\frac{2}{9} \left( \frac{1}{m^2} + \frac{1}{mm_s^2} \right), \quad \omega_d^{(2)}(1) = -\frac{2}{27} \left( \frac{2}{m^2} - \frac{1}{mm_s^2} \right) \quad (A16) \]

3. Contact spin-spin

\[ V_D^{ss}(\vec{p}, \vec{p}') = \kappa_{ss} \omega_D(I) \eta_D \exp \left[ -A_D p^2 - B_D p'^2 + C_D \vec{p} \cdot \vec{p}' \right] \quad (A17) \]

Diagram (a):

\[ A_a = \frac{2(1 + \rho)^2 + 3g}{12\alpha^2(1 + \rho)^2}, \quad B_a = A_a, \quad C_a = \frac{2(1 + \rho)^2 + 3g}{6\alpha^2(1 + \rho)^2} \]

\[ \eta_a = 1, \quad \omega_a(1) = 1/3, \quad \omega_a(0) = 0 \]

\[ \omega_a(1) = 1/3, \quad \omega_a(0) = 0 \]

Diagram (b):

\[ A_b = \frac{(5g + 3)\rho^2 + (-2g + 6)\rho + (2g + 3)}{6\alpha^2(g + 3)(1 + \rho)^2}, \quad B_b = \frac{(5g + 3)\rho^2 + (10g + 6)\rho + (5g + 3)}{6\alpha^2(g + 3)(1 + \rho)^2} \]

\[ C_b = \frac{(1 - g)\rho^2 + 2\rho + (g + 1)}{\alpha^2(g + 3)(1 + \rho)^2} \]

\[ \eta_b = \rho \left( \frac{6}{g + 3} \right)^{3/2}, \quad \omega_b(1) = 1/3, \quad \omega_b(0) = 0 \]

Diagram (c):
\[ A_c = \frac{(16g + 3)\rho^2 + (2g + 6)\rho + (21g^2 + 22g + 3)}{12\alpha^2 (7g + 6)(1 + \rho)^2} \]
\[ B_c = \frac{(64g + 3)\rho^2 + (62g + 6)\rho + (21g^2 + 34g + 3)}{12\alpha^2 (7g + 6)(1 + \rho)^2} \]
\[ C_c = \frac{(1 - 8g)\rho^2 + 2\rho + (7g^2 + 8g + 1)}{2\alpha^2 (7g + 6)(1 + \rho)^2} \]
\[ \eta_c = \left( \frac{12g}{7g + 6} \right)^{3/2} \quad \omega_c(1) = 1/18 \quad \omega_c(0) = 1/6 \]

Diagram (d):
\[ A_d = \frac{(20g^2 + 40g + 3)\rho^2 + (4g^2 + 14g + 6)\rho + (5g^2 + 10g + 3)}{12\alpha^2 (2g + 3)(g + 2)(1 + \rho)^2} \quad B_d = A_d \]
\[ C_d = \frac{(1 - 4g^2 - 8g)\rho^2 + (2 - 4g^2 - 6g)\rho + (g^2 + 2g + 1)}{2\alpha^2 (2g + 3)(g + 2)(1 + \rho)^2} \]
\[ \eta_d = \rho \left[ \frac{12g}{(2g + 3)(g + 2)} \right]^{3/2} \quad \omega_d(1) = 1/18 \quad \omega_d(0) = 1/6 \]

4. Contact spin-independent

\[ V_D^{\text{Con-SI}}(\vec{p}, \vec{p}') = 4\pi\alpha_s \omega_D(I) \exp \exp \left[ -A_D p^2 - B_D p'^2 + C_D \vec{p} \cdot \vec{p}' \right], \quad (A18) \]

where the functions \( A_D, \cdots \) are the same as for the spin-spin interaction and
\[ \omega_a(1) = + \frac{1}{9} \frac{1}{m^2} \quad \omega_a(0) = 0 \]
\[ \omega_b(1) = - \frac{1}{18} \frac{1}{m^2} (1 + \rho^2) \quad \omega_a(0) = 0 \]
\[ \omega_c(1) = - \frac{1}{9} \frac{1}{m^2} \quad \omega_a(0) = 0 \]
\[ \omega_c(1) = - \frac{1}{18} \frac{1}{m^2} (1 + \rho^2) \quad \omega_a(0) = 0 \quad (A19) \]

5. Confinement

The confining interaction is taken to be a linearly rising potential, which in momentum space is given as
\[ V_{\text{conf}} = \frac{6\pi\sigma}{q^4}, \quad (A20) \]

where \( \sigma \) is the string tension. Eq. (A20) includes a color factor of \( 3/4 \). The effective \( KN \) interaction is given by
\[ V_{D}^{\text{Conf}}(\vec{p}, \vec{p}') = 6\pi \sigma \omega_D(I) \int_{0}^{\infty} du \int_{u}^{\infty} ds \eta_D(s) \exp \left[ -A_D(s) p^2 - B_D(s) p'^2 + C_D(s) \vec{p} \cdot \vec{p}' \right], \]

(A21)

where the functions \( A_D(s), B_D(s), C_D(s) \) and \( \eta_D \) are the same as for the Coulomb term, and the \( \omega_D(I) \)'s are given by:

\[
\begin{align*}
\omega_a(1) &= +4/9 \quad \omega_a(0) = 0 \\
\omega_b(1) &= -4/9 \quad \omega_b(0) = 0 \\
\omega_c(1) &= -4/9 \quad \omega_c(0) = 0 \\
\omega_d(1) &= +4/9 \quad \omega_d(0) = 0.
\end{align*}
\]
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TABLE I. Vertex parameters used in the Jülich $KN$ model I [2]. Numbers in parentheses denote corresponding values of the model discussed in the present paper, when different.

| Process       | Exch. part. | $M_r$ or $m_r$ $^{a)}$ [MeV] | $g_1 g_2/4\pi$ $^{b)}$ [$f_1/g_1$] | $\Lambda_1$ $^{c)}$ [GeV] | $\Lambda_2$ $^{c)}$ [GeV] |
|---------------|-------------|-------------------------------|-----------------------------------|-----------------------------|-----------------------------|
| $KN \rightarrow KN$ | $\sigma$ | 600 | 1.300 | 1.7 | 1.5 |
|                | $\sigma_{rep}$ | 1200 | -40 | 1.5 | 1.5 |
|                | $a_0$ | 980 | (-) | (-) | (-) |
| $KN \rightarrow K^*N$ | $\omega$ | 782.6 | 2.318 | 1.5 | 1.5 |
|                | $\rho$ | 769 | 0.773[6.1] | 1.4 | 1.6 |
| $KN \rightarrow K^*\Delta$ | $\Lambda$ | 1116 | 0.905 | 4.1 | 4.1 |
|                | $\Sigma$ | 1193 | 0.031 | 4.1 | 4.1 |
|                | $Y^*$ | 1385 | 0.037 | 1.8 | 1.8 |
| $KN \rightarrow K\Delta$ | $\pi$ | 138.03 | 3.197 | 1.3 | 0.8 |
|                | $\rho$ | 769 | 0.773[6.1] | 1.4 | 1.0 |

$^{a)}$ Mass of exchanged particle.

$^{b)}$ Product of coupling constants [ratio of tensor to vector coupling].

$^{c)}$ Cutoff mass.
FIGURES

FIG. 1. Meson-exchange contributions to $KN$ scattering in the Jülich model [1,2]. Diagrams (a) and (b) define the model of Ref. [1] and diagram (c) is the correlated $2\pi$ exchange calculated in Ref. [2], which was parametrized by diagram (a) in Ref. [1].

FIG. 2. The four quark-interchange kaon-nucleon scattering diagrams.

FIG. 3. $KN$ phase shifts. The solid line are the result from the full quark-model calculation described in the text. Experimental phase shifts are taken from Ref. [16] (open circles), Ref. [17] (open squares), and Ref. [18] (filled circles and pluses).

FIG. 4. $KN$ phase shifts resulting from various contributions of the quark model, cf. Appendix A: Coulomb (dash-dotted line); Spin-orbit (pluses); Confinement (short dashed line); Contact spin-spin (long dashed line); Contact constant (solid line).

FIG. 5. $KN$ phase shifts. The dash-dotted line are the phase shifts of the original Jülich model I from Ref. [2]. The short dashed line shows results where the phenomenological $\sigma_{\text{rep}}$ in the Jülich model is replaced by the quark-model contribution. Adding the $a_0$-exchange contribution yields the long dashed line. The solid line is obtained after refitting the parameters of the $\sigma$. Same description of experimental phase shifts as in Fig. 3.
Fig. 1
Fig. 2
Fig. 3
Fig. 4
Fig. 5
Fig. 5, cont.
Fig. 5, cont.
Fig. 5, cont.