1. Introduction

There are a variety of approaches to estimate above ground biomass (AGB), which can be classified according to the data source being used (Koch and Dees, 2008): field measurement, remotely sensed data or ancillary data used in GIS-based modeling. Field measurements are based on destructive sampling or direct measurement and the application of allometric equations (Madgwick, 1994). Recently, remotely sensed data, from both passive and active sensors, have become an important data source for AGB estimation. In this chapter we will focus on the use of optical multispectral data such as TM/ETM+ to estimate AGB. Generally, biomass is either estimated via a direct relationship between spectral response and biomass using multiple regression, k-nearest neighbor, neural networks, inverse canopy models or through indirect relationships, whereby attributes estimated from the remotely sensed data, such as leaf area index (LAI), structure (crown closure and height) or shadow fraction are used in equations to estimate biomass (Wulder, 1998). Here, we discuss the use of remote sensing data of moderate spatial resolution as input to estimate AGB. Research has demonstrated that it is more effective to generate relationships between field measurements and moderate spatial resolution remotely sensed data (e.g., LANDSAT), and then extrapolate these relationships over larger areas using comparable spectral properties from coarser spatial resolution imagery (e.g., MODIS) (Steininger, 2000; Lu, 2005; Phua and Saito, 2003; Foddy et al., 2003; Fazakas et al., 1999; Roy and Ravan, 1996; Zheng et al., 2004; Mickler et al., 2002). In general terms, LANDSAT TM and ETM+ data are the most widely used data of remotely sensed imagery for forest biomass estimation, but data from other moderate spatial resolution sensors have also been used, including ASTER and HYPERION data. In this chapter we present approaches that are currently being developed in Chile. Specifically, we introduce methods for the estimation of AGB using medium spatial resolution satellite imagery and digital elevation models. The main objective is to create, calibrate and validate such methods for applications. We developed an alternative approach in the estimation of AGB using LANDSAT ETM+ imagery and SRTM digital elevation models as covariates for geostatistical modeling. From the spatial perspective, AGB data correspond to an array of points in space (x, y), while covariates correspond to a set of data that has a large number of samples in geographic space (extracted from each pixel), some of which having overlap with the available AGB.
data. The method can estimate the spatial variation of AGB at a stand or sub-stand level, and measure the uncertainty attached to the estimation, depending on local conditions. These results are promising and demonstrate the feasibility of using this approach in the evaluation and monitoring of stock biomass or communal farm scale. They are applicable to the actual landscape configuration of the country, open a series of new interest in research and development, and constitute a novel way to solve the problem of assessing biomass stocks.

2. Multispectral data for forest biomass estimation

Some remote sensing studies using LANDSAT TM/ETM + imagery have focused on estimating the forest attributes through correlation or regression analysis with the spectral response obtained from the images. The estimated attributes may include basal area, AGB, canopy closure, diameter at breast height (DBH), tree height, stand density, and leaf area index (LAI) (Franklin, 1986; Horler and Ahern, 1986; Peterson et al., 1986 and 1987; Lathrop and Pierce, 1991; Ardo, 1992; Curran et al., 1992; Cohen and Spies, 1992; Gemmell, 1995; Kimes et al., 1996; Trotter et al., 1997; Turner et al., 1999; Eklundh et al., 2001; Lu et al., 2004; Hall et al., 2006). One of the methods used to estimate attributes of forests from LANDSAT imagery is the direct correlation with radiometric values where regression relationships can be calculated between spectral bands, band ratios or vegetation indices (Franklin, 1986; Roy and Ravan, 1996; Jakubauskas and Price, 1997; Foody et al., 2003; Labrecque et al., 2006). The most used way to perform this kind of method is by applying stepwise forward variable selection. Table 1 summarizes some studies using this method in several countries.

Some of the advantages of using remotely sensed data are through the provision of a synoptic view of the study zone, capturing the spatial variability in the attributes of interest such as biomass, dominant height or crown closure (Zhen et al., 2007). Remotely sensed data can also be used to fill spatial and temporal gaps in forest inventory attributional data, improving estimates of forest biomass and carbon stocks, which can done for large areas as they are not limited by the extent of forest inventories (Birdsay, 2004; Fournier et al., 2003). However, the complicated vegetation stand structures in mature forest and in advanced successional forests often make the results less accurate given similar TM reflectance even if the above ground biomass varies significantly. This disadvantage is often called data saturation. For instance, in Manaus (Brazil) the canopy reflectance of tropical secondary successional forests saturated when AGB approached about 15 kg m-2 or vegetation age reached over 15 years (Steininger, 2000). Nelson et al. (2000) analyzed secondary forest age and AGB estimation using Landsat TM data and found that AGB cannot be reliably estimated without the inclusion of secondary forest age. The main approach to overcome this problem is to include further co-variables independent to reflectance values. The k-NN method has become popular for forest inventory mapping and applications of estimation over the last years (McRoberts et al., 2007; McRoberts and Tomppo, 2007; Bafetta et al., 2009; Tomppo et al., 2009; Maselli et al., 2005; Tomppo and Halme, 2004; Thessler et al., 2008). The basic idea of this method is to estimate a target attribute of an object, i.e. AGB, using its similarity to objects with known attributes. Its application has focused on estimating continuous variables such as size, age, height, basal area, mean DBH, standing volume, and leaf area (Tomppo et al., 2009; McRoberts et al., 2007; Bertini et al, 2007; Tomppo and Halme, 2004).
Table 1. Examples of methods using LANDSAT data for estimation of forest biomass.

| Sensor | Study area | Estimation method | References |
|--------|------------|-------------------|------------|
| TM 5   | Manaos, Brazil | Lineal and exponential regression | Steininger (2000) |
| TM 5   | Pará state and Rondônia, Brazil | Multiple regression | Lu (2005) |
| TM 5   | Sabah, Malaysia | Exponential regression | Phua and Saito (2003) |
| TM 4 and 5 | Man aos, Brazil; Danum Valley, Malaysia; Khun Kong, Thailand | Multiple regression and neural network analysis | Foddy et al. (2003) |
| TM 5   | Sweden | K nearest neighbor (k-NN) | Fazakas et al. (1999) |
| TM 5   | Madhav National Park, India | Multiple regression | Roy and Ravan (1996) |
| ETM+   | Wisconsin, USA | Multiple regression | Zheng et al. (2004) |
| ETM+   | Southwest USA | PnET productivity model | Mickler et al. (2002) |

3. Estimation of biomass in Chilean forests

Estimation studies of forest biomass in Chile began to appear in the late 80’s, primarily for plantation of *Pinus radiata* (Caldentey, 1989) and, subsequently, for some local native species (Caldentey, 1995; Garfias, 1994; Herrera and Waisberg, 2002; Schlegel, 2001; Schmidt et al., 2009). In native forest, the background data is limited. The estimation method to be applied depends on the forest composition, structure, and site variability. Natural forests are highly variable in these attributes (Donoso, 1993; Gajardo, 1994; Luebert and Pliscoff, 2006) while plantations have less variation because they are monospecific and grow under intensive management regimes, designed to standardize the size and the quality of all trees (Lewis and Ferguson, 1993; Lavery, 1986; Gerding, 1991; Toro and Gessel, 1999). Secondary native forests, especially those dominated by the genus *Nothofagus*, have an intermediate degree of variation and heterogeneity (Donoso, 1981; Donoso, 1993; FIA, 2001). Traditionally, AGB estimation methods are based on sampling methods designed to assess standing timber (Husch et al., 1993; Anuchin, 1960; Bitterlich, 1984, Avery and Burkhart, 1994; Loetsch et al., 1973; Prodan et al., 1997). There is no reason for a different design because the volume/biomass ratio is relatively constant mainly depending on wood density. For the same reason, existing inventory plots can be used to estimate AGB directly. The AGB estimation method, which is usually performed for trees larger than 5 cm in diameter at breast height (DBH) and the understory is not included, should be done taking the following steps:

a. Estimate AGB at individual tree level. Given the high cost of measuring the biomass into its components (stem, bark, branches and leaves) it is preferable to use existing allometric equations for biomass by species and component. These equations depend on easy-to-measure state variables (i.e. DBH and height (H)) and allow estimating AGB in similar trees within the stand (Keith et al., 2000; Wang, 2006; Baker et al., 1984; Ares and Braener, 2005; Zewdie et al., 2009; Ketterings et al., 2001). The biomass components are estimated based on basic density samples (dry weight / green volume) multiplied by the total volume of the component (Keith et al., 2000; Steininger, 2000; Ishii and Tatedo, 2004; Hall et al., 2006). All these functions have the following generic form:
\[ B^c_i = f(DBH_i, H_i, S_i) + \xi_i \]

where:
- \( B^c_i \) is the biomass of component \( c \) in the \( i^{th} \) tree
- \( DBH_i \) is the diameter at breast height of the \( i^{th} \) tree
- \( H_i \) is the total height for the \( i^{th} \) tree
- \( S_i \) is an estimator of the sound/dead biomass proportion of the \( i^{th} \) tree
- \( \xi_i \) is the regression error of the \( i^{th} \) tree

(1)

b. Estimation of AGB for areal units. To this end, one has to use sampling plots within the target units and then their statistics as the estimates. In order for this to work properly, it is necessary to measure DBH, species and some health variable of the tree (usually subjective). In natural forests, due to the high variability for trees having the same DBH range, it is better make measurements of \( H \) and \( S \) in order to improve the precision of the results. In plantations (more homogeneous forests) the same can be made by applying a subsample for \( H \) and then to estimate the rest using a regression model for \( H \) as a function of the DBH.

The estimated AGB at plot level has the following generic form:

\[ B^c_j = \sum_{i=1}^{n_j} B^c_{ij} \times F_j \]

where:
- \( B^c_j \) is the biomass of the component \( c \) for the \( j^{th} \) plot (ton/ha)
- \( n_j \) is the number of trees in the \( j^{th} \) plot
- \( F_j \) is the hectare expansion factor for the \( j^{th} \) plot

(2)

c. Estimation of biomass at the stand, local, regional or national levels. The scales of interest for estimating AGB ranges from stand up to national levels according to the scale of the project. From stand level estimations the other aggregation levels can easily be archived by simply adding other stands estimation into the calculation. The biomass estimate at stand level has the following generic form:

\[ B^c_r = a \sum_{k=1}^{m} B^c_k \times \frac{1}{m} \]

where:
- \( B^c_r \) is the biomass of the component \( c \) for the \( r^{th} \) stand (ton)
- \( a \) is the total area of the stand (ha)
- \( m \) is the number of plots within a the stand

(3)

The use of optical satellite and topography data as auxiliary variables (covariables) allow the accuracy of AGB estimations to improve because they are based on their spatial covariation to field data by applying geostatistical interpolation. Using topographic data, the AGB variation is scaled to the actual values for that area, and then, AGB can be obtained by overlaying any available administrative division (stands, sites or districts).
Fig. 1. Alternative AGB estimation based on the type of the available data.

According to the available data one can use different methods to estimate AGB (Figure 1). If data are traditional forest inventory plots, estimates should be made by using traditional statistical parameters for total and average quantities, which don’t give any explicit information about the spatial variability of forest attributes. If data are georeferenced, distributed in such a way that they represent the whole territory of interest, then a spatial interpolation method, such as inverse distance interpolation or kriging, can be applied. The former approach has the advantage of being an unbiased probabilistic method where the degree of confidence (accuracy) can be calculated. The basic assumption behind kriging interpolation is that the spatial dependence models described in variograms assume the behavior of a regionalized variable, which is not necessarily true in reality and should be proved. On the other hand, if it is possible to have other variables (covariates), which besides being cheaper to obtained, are spatially well correlated to the variable of interest (AGB), then they can used to somehow correct the weakness of kriging by accounting for spatial discontinuities or irregularities found in nature (Coulston, 2008).

3.1 Native forest description

Chilean forests cover an area of 15.6 million hectares (20.7% of the national territory), of which 13.4 million hectares are natural forests (85.9% of the forested area). Currently 3.6 million hectares of forest are secondary forests (CONAF et al., 1999). Mixed forest of *Nothofagus obliqua*, *Nothofagus alpina* and *Nothofagus dombeyi* are one of the most important forest types in the country and cover 1.5 million hectares (12.2% of the total native forest). The genus *Nothofagus* has ten species that have a high economic value because of the quality of their wood. These *Nothofagus* forests area concentrated between 36° 30' S and 40° 30' S and between 100 and 1,000 m a.m.s.l. in Central Chile. They are present in both mountain ranges, costal and the Andes, where *N. obliqua* occupies the lowest areas (between 100 and 600 m, approximately), *N. alpina* intermediate ones (between 600 and 900 m) and *N. dombeyi* the highest (between 900 and 1,000 m), resulting in overlap ecotones with pure and mixed formations (CONAF et al., 1999; Donoso, 1981; Gajardo 1994). The main secondary species in these mixed *Nothofagus* second growth forest are *Aextoxicon punctatum*, *Genuine avellana*, *Laurelia sempervirens*, *Persea lingue* and *Eucryphia cordifolia* (Donoso, 1981). Today, a major part of these forests exhibit some state of degradation or have some form of human perturbation (Donoso, 1981; Gajardo, 1994). Nevertheless, they have a high productive potential and they need to be managed to improve their current condition. Usually, the quantification of these resources is done by applying volume tables or biomass functions, but these biomass functions rarely exist for native species and have only local applications.
(Caldentey, 1995; Donoso et al., 2010; Garfias, 1994; Gayoso et al., 2002; Herrera and Waisberg, 2002; Sáez, 1991; Schlegel, 2001, Schmidt et al., 2009) (see Table 2). For native species, the biomass estimation methods most used in Chile are regression or allometry for the average tree (see section 3.0). In recent years, further attention has been paid in less expensive methods to assess AGB in native forests, based on remote sensing data and spatially explicit methods (Peña, 2007; Valdez et al., 2006).

3.2 Plantation description

In Chile, forest plantations are the main supply source of industrial raw material, with a total of near 40 million cubic meters. *Pinus radiata* D. Don is the main commercial species behind these massive commercial activities, with 80% of participation, followed by eucalyptus with 20% participation (CORMA, 2011). The plantations are concentrated in the central coastal area of Chile, between latitude 32° S and 42° S (Figure 2), covering a wide range of soils types (Schlatter, 1977; Schlatter and Gerding, 1984), environmental conditions (Fuenzalida, 1965; Madgwick, 1994) and silvicultural management regimes (Lewis and Ferguson, 1993; Lavery, 1986; Gerding, 1991). The land ownership structure is highly concentrated in two large forestry companies, which together owned 53% of the total planted area (CNE, GTZ / INFOR, 2008; Leyton, 2009), and the problem of quantifying wood supply has been primarily addressed by the private sector. Therefore, little public information exists on the area, location, age, species and management regime of plantations (CORMA, 2011). In contrast, the private sector has a large network of forest inventory information and has built growth simulators for the main species for different areas (i.e. *Radiata* and *Eucasia* models), types of site and management schemes and bucking (Fundación Chile, 2005; Morales et al., 1979). Some studies on the availability of wood for the forest industry (CORMA, 2011), carbon sequestration by plantations (Gilabert et al., 2010), AGB stocks for energy projects (INFOR, 2010, CNE / GTZ / INFOR, 2008) have been made by combining regional forest inventory data and these simulation models.

| Chile Region | Forest Type | AGB (Mg/ha) | Author            |
|--------------|-------------|-------------|-------------------|
| VIII         | *N. alpina* second growth forest | 104         | Garfias, 1994     |
| X            | Evergreen   | 194 to 663  | Schlegel, 2001    |
| X            | Mixed *N. obliqua, N. alpina* and *N. dombeyi* | 285         | Herrera and Waisberg, 2002 |
| XII          | *Nothofagus pumilio* | 380 to 447  | Caldentey, 1995   |

Table 2. Above ground biomass of different types of forest and locality.

4. Remote sensing based biomass estimation

4.1 Description of the study areas and field data collection

We consider four study areas, two predominantly plantations (pine and eucalyptus) and two covered with mostly second growth Chilean oaks: *Nothofagus obliqua, Nothofagus alpina* and *Nothofagus dombeyi*. In both cases, one of the areas has a farm spatial scale and the other a municipality level (Table 3). Figure 2 shows the geographic location of the four areas of study.
Geostatistical Estimation of Biomass Stock in Chilean Native Forests and Plantations

| Forest type                  | Study area | Ha   | Description                                                                 |
|------------------------------|------------|------|-----------------------------------------------------------------------------|
| Plantations                  | Pantanillos| 400  | Mainly Pinus radiata and few Eucaliptus globulus stands, both at different ages with intensive management. |
|                              | Quivolgo   | 20 000 | Mainly N. obliqua with several secondary tolerant species and informal management. |
| Native, secondary forest     | Monte Oscuro | 1 600 | Mixed of N. obliqua, N. Alpina, N. dombeyi at different ages and without management. |
|                              | Curacautín | 20 000 |                                                                                   |

Table 3. Description of the study areas

We used a random sampling design and concentric circular sampling units (8m radius). All the data were collected in summer 2010 and the total size of the sampling was 348 plots, with an average sampling intensity of one sampling units every 63.2 hectares. Each selected tree was measured for DBH and one out of three for total height (H). For young plantations where understory foliage did not allow seeing trees at DBH we used circular plots with a radius of 5.65 m. In plantations stands where individuals grew in clusters - coppice type - we counted the number of individuals per unit and DBH and H was measured for the smaller and bigger trees. Biomass calculations were performed using the methods presented in Section 3.

4.2 Methods

4.2.1 ETM+ and SRTM data acquisition and preprocessing

LANDSAT ETM+ images were obtained from the Earth Explorer Web site of the United States Geological Survey (USGS). Additionally, the SRTM digital elevation model (90 m) was freely downloaded from the site Earth Explorer. Bands ETM+ 1, 2, 3, 4, 5 and 7 were grouped into a single file and then projected to WGS84 UTM 18 South or 19 South, according to the area to which they correspond. Subsequently, there were a series of preprocessing steps as detailed below:

a. SLC-off Correction: The images acquired after 2003 have missing data due to malfunction of an instrument called Scan Line Corrector (Figure 3). This so-called SLC-off error was corrected using ENVI® software application, which fits the flaw by using two images with the error in different areas, i.e. non-overlapping. Interpolation is performed considering the local histogram of the two images.

b. Geometric Correction: The images were rectified using Chilean regular cartography 1:50.000 with at least 30 control points per image and a root mean square error less than 30 m was achieved.

c. Radiometric corrections: Standard radiometric corrections were applied on all images to reduce the atmospheric effect following the method proposed by Chavez (1996), and for the topographic the one proposed by Riaño et al. (2003).

Once ETM+ and SRTM were co-registered, several variables were then derived:

a. Normalized Difference Vegetation Index or NDVI (Tucker, 1979).

b. Tasseled Cap bands: Brightness (TC1), Greenness (TC2) and Wetness (TC3). The other three components (TC4, TC5 and TC6) do not have a direct biophysical interpretation but were also calculated to take into account the complete data variation.

c. Slope, Aspect and Altitude were directly calculated from SRTM data.
Fig. 2. Forest resources in Chile and geographical location of the study areas.
4.2.2 Data integration

The integration of all layers of information was carried out in GIS environment (ArcGIS 9.3\textsuperscript{RM}) and grouped into four classes:

a. Field data, which contain the observed AGB (target variable) and its coordinates.

b. ETM spectral bands, excluding the thermal band, plus their derivatives: NDVI and Tasseled Cap components (covariates).

c. Topographic information derived from SRTM data: elevation, slope, and orientation (covariates).

d. Vector files with property boundaries, stands, and base cartography support, which are useful in the stratification of the results and administrative aggregation.

For each of the four study areas a database was generated, which was used subsequently in the geostatistical analysis. Data were treated as point processes or count variables in the bi-dimensional space. Each set of field data is associated with a specific geographical area, for which all values to a resolution of 16 or 30 meters were considered in a comprehensive manner. Figure 4 shows the general methodological approach and the generic structure of the databases for each area.

From here and for the remaining sections, we considered biomass and all covariates mentioned above as regionalized variables to be able to follow the formality of geostatistical analysis. First, we performed a variogram analysis with the aim of studying the spatial autocorrelation of biomass and its spatial dependence with covariates. The result is a set of spatial models called variograms for the variable of interest (biomass) and the covariates. In all cases, we analyzed the anisotropy of the models, incorporating it explicitly in subsequent interpolations whenever possible. The variograms were used in the spatial estimation of biomass via cokriging. The exploratory analysis and modeling process were performed using Isatis\textsuperscript{RM} geostatistical software and Matlab\textsuperscript{RM} environment.
4.2.3 Variogram analysis

The values of a regionalized variable such as biomass are not independent, in the sense that the value observed in a site provides information about the values of neighboring sites (i.e. one is more likely to find a high value of biomass near other high values). In the geostatistical interpretation of the regionalized variable this intuitive notion of dependence is described by the formulation of random functions, which model the way the values observed in different sites relate to each other by a multivariate probability distribution.

The moment of order 1 of a random function (expected value or mean) involves a single spatial position and does not actually deliver information on spatial dependence. In contrast, the moments of order 2 (especially, the variogram) are defined with the help of two spatial positions, i.e. the smallest set that can be considered to describe the spatial "interaction" between values. These are the moments that give a basic description and operations of the spatial continuity of the regionalized variable.

Variogram analysis consists in calculating an experimental variogram from the available data, and subsequently fitting a theoretical variogram model. The experimental variogram measures the mean squared deviation between pairs of data values, as a function of the separation vector (distance and orientation) between the two data. The characteristics of this variogram are related to the characteristics of the regionalized variable (Isaaks and Srivastava, 1989; Chilès and Delfiner, 1999), in particular:

a. The behavior of the variogram near the origin reflects the short-scale variability of the variable.

b. The increase of the variogram reflects the loss of spatial correlation with the separation vector. It may depend on the direction of this vector, indicating the existence of directions with greater spatial continuity than others (anisotropy).

c. The range of correlation, for which the variogram reaches a sill (plateau), indicates the distance at which two data do no longer have any correlation.

In practice, the anisotropy can be identified by comparing experimental variograms calculated along various directions of space, for example oriented 0°, 45°, 90° and 135° with respect to the x-axis. Often, this test is completed by drawing a “variogram map”. When there is isotropy, the experimental variograms in different directions overlap and concentric circles are drawn in the variogram map. Otherwise, one may distinguish geometric anisotropies, in which the variogram map draws concentric ellipses; in such a case, the modeling rests upon the experimental variograms along the main anisotropy axes, which correspond to the axes of the ellipses.
Once calculated, the experimental variogram is fitted with a theoretical model, which usually consists of a set of basic nested structures with different shapes, sills and/or ranges (Gringarten and Deutsch, 2001). Examples of basic structures include the nugget effect (discontinuous component), as well as the spherical, exponential, cubic, Gaussian and power models (Chiles and Delfiner, 1999).

In the multivariate case, one has to calculate the experimental variogram of each variable (direct variogram), as well as the cross-variograms between each pair of variables, which measure the spatial correlation structure of the set of coregionalized variables. The fitting of a nested structure model is subject to mathematical constraints, reason for which one usually resorts to automatic or semi-automatic fitting algorithms (Wackernagel, 2003).

4.2.4 Interpolation by kriging

Kriging aims at estimating the value of the regionalized variable (here, AGB) at a position with no data, as accurately as possible, using the data available in other positions. It is structured according to the following steps:

a. Linearity constraint: The estimator must be a linear combination (i.e., a weighted average) of the data.

b. Unbiasedness constraint: This step expresses that the expected error is zero: if one considers a large number of identical kriging configurations, the average estimation error approaches zero. The absence of bias does not guarantee that errors are small, only that they cancel out on average.

c. Optimality constraint: according to the above steps, the estimator is subject to one or more constraints but is not fully specified. The last step consists in minimizing the estimation error variance, which measures the dispersion of the error around its zero mean, therefore the uncertainty in the true unknown value. Intuitively, this restriction means that if a large number of identical kriging configurations are considered, the statistical variance of the estimation errors is as small as possible. In addition to the estimated value, one can also calculate this minimal estimation error variance, known as the “kriging variance”.

The weighting of the data depends on the spatial continuity of the regionalized variable, as modeled by the variogram, and on the spatial configuration of the data and location to estimate. In general, closer data receive larger weights than data located far from the target location, but this may be counterbalanced by other effects. For instance, data that are clustered in space tend to convey redundant information and may therefore receive small weights; data located along directions of little spatial continuity (with a small variogram range) may also be underweighted with respect to data located along directions of greater continuity.

There exist many variants of kriging, depending on the assumptions about the first-order moment or mean value (in particular, whether it is known or not, constant in space or not) and on the areal support of the value to estimate (“point” support identical to that of the data, or “block” support larger than that of the data) (Chiles and Delfiner, 1999). The multivariate extension of kriging is known as cokriging, which makes use not only of the data of the variable to estimate (primary variable), but also of covariates that are cross-correlated with this primary variable (Wackernagel et al., 2002). The determination of cokriging weights and of the error variance relies on the set of modeled direct and cross variograms (Wackernagel, 2003).
4.2.5 Kriging and cokriging neighborhood

Quite often, the amount of available data is large and using all of the available data is impractical and a selection of the most relevant data is required. One therefore defines a local window or “kriging neighborhood” in which to search for nearby data and to perform local estimation. The shape of the neighborhood should explicitly consider the detected anisotropies, by making the search radius dependent on the variogram range: the larger the range along a direction, the larger the search radius. Typically, the neighborhood is defined by placing an ellipse around the target location, and selecting a given number of data within this ellipse. The justification for such a practice is the so-termed screening effect, according to which the closest data screen out the influence of farthest data (David, 1976; Stein, 2002). Also, to avoid the selection of clustered data that convey redundant information, it is good practice to divide the neighborhood into several angular sectors (e.g., quadrants or octants) and to look for data within each sector (Isaaks and Srivastava, 1989).

Such a definition of the kriging neighborhood is, however, mainly heuristic and one is usually not aware of which data are really worth being included in the neighborhood, and which data can be discarded without deteriorating the estimation. The optimal neighborhood actually depends on the variogram of the variable of interest, as the screening effect does not occur with every variogram model. Some generic guidelines have been provided by Rivoirard (1987) to validate the choice of a given neighborhood in the univariate context.

In the multivariate case, the design of the neighborhood is more complex and critical. For instance, the data of a covariate may be screened out by the collocated data of the primary variable or, on the contrary, they may supplement the primary data and provide useful information to improve local estimation. As suggested by recent publications (Rivoirard, 2004; Subramanyam and Pandalai, 2008), the decision to include or not the covariate data should consider the correlation structure of the coregionalized variables and the sampling scheme (in particular, whether or not all the variables are measured at all the sampling locations). Some options include:

a. Single search: the data points are selected according to their proximity to the target location, irrespective of which variable(s) is (are) informed at these data points.

b. Two-part search: the first one is a selection of the nearby data of the primary variable, ignoring the information of covariates; the second one is a selection of the nearby data of the covariates, ignoring the information of the primary variable. The advantage of this strategy is to decouple the search of data according to the nature of the variable (primary or covariate). The disadvantage is that the search and the resolution of the cokriging equations must be carried out as many times as there are variables to estimate.

4.3 Results

4.3.1 Selection of variables

To estimate AGB we used ordinary cokriging (i.e., cokriging with unknown means that are assumed constant at the scale of the neighborhood) considering all the available covariates. Cokriging only works with linearly independent variables, for which there is no colinearity or "redundancy" of information. For this reason, the spectral bands TM1 to TM7 were excluded from the analysis since these variables can be deduced from that of the other variables such as Tasseled Cap components and NDVI. Also, the orientation variable
corresponds to an angle between 0 and 360 degrees, so the value 0 represents the same information as the value 360. In order to prevent very different values to represent equal or nearly equal angles, we replaced the angles by their cosines and sines. Thus, in addition to the primary variable (AGB), we used the following 11 covariates in all the analyses: altitude (ALT), orientation cosine and sine (ASPECT), slope (SLOPE), normalized difference vegetation index (NDVI), and the six Tasseled Cap components (TC1, TC2, TC3, TC4, TC5 and TC6).

4.3.2 Variogram analysis
While there is much information from the covariates (tens of thousands to millions of records) from which experimental variograms can be calculated in a very detailed way, information is scarcer with the primary variable (AGB) that has only a few hundreds of positions with field data. Because of the limited data available for the country, the inference of the variograms of the primary variable and the cross variograms between this variable and all covariates is difficult. To determine the spatial correlation structure, we chose one of the following alternatives, depending on the case under study:

a. Use of traditional experimental directional variograms, calculated along the identified main directions of anisotropy (Pantanillos case study).
b. Use of omnidirectional variograms, when anisotropy was not detectable for the primary variable (AGB) due to the scarcity of data (Quivolgo and Curacautín case studies).
c. Use of centered covariance as a substitute to the variogram (Chilès and Delfiner, 1999) in case the experimental variogram is too erratic (Monte Oscuro case study).

As an illustration, Figure 5 shows the experimental and modeled variograms for AGB, Brightness (TC1), Greenness (TC2) and Wetness (TC3), along the two identified main directions of anisotropy (north-south N0ºE and east-west N90ºE), for the Pantanillos area. For TC1, TC2 and TC3, the spatial variability appears to be greater along the north-south direction than along the east-west. These direct variograms, together with that of the other covariates and with the cross-variograms (a total of 78 variograms), have been jointly fitted thanks to the algorithm proposed by Goulard and Voltz (1992), using a nugget effect and nested exponential and power basic structures.

4.3.3 Cokriging neighborhood definition and application
To run cokriging, it is also necessary to define a neighborhood containing the data relevant to the local estimation. Given the very different number of data between the variables (AGB with very few data in comparison with covariates), we decided to use a two-part search:

a. For AGB we considered the 15 closest available data.
b. For each covariate, the 50 closest data were considered.

Cokriging was performed with an ad hoc MATLAB routine, since no known commercial software is able to perform cokriging with the above specifications and 11 covariates. The results are estimated values and error variances for AGB. The estimates were made for all the study areas, at the nodes of a grid with cells of 16m × 16m or 30m × 30m, depending on the case study, assuming unknown mean values for all the variables (ordinary cokriging). Since not all the land in each area is covered by vegetation, we subsequently multiplied the estimates and error variances by the fraction of the cells located inside the identified stands, using vector digital layers of their boundaries. Figures 6 and 7 present the field data and identified stands, as well as the cokriging results for the Pantanillos area.
Fig. 5. Experimental (dots and dashed lines) and modeled (solid lines) variograms along the directions N0°E (black) and N90°E (blue) for AGB (top left), TC1 (top right), TC2 (bottom left) and TC3 (bottom right) in Pantanillos study area.
4.4 Conceptualizing and generalizing the method
The estimation approach we developed is a real alternative for assessing AGB at communal and regional scales. It has a relatively low implementation costs when compared to traditional methods (i.e. inventories of land) and can be used to assess and monitor the stock of biomass over time on a country-wide scale. Although it requires field data, it is possible to estimate other areas using the already gained knowledge (in particular, the spatial correlation structure, via the direct and cross variogram models). The idea is based on two hypotheses:

a. The amount of biomass available at any point in the geographical space depends, first, on the productivity of the site and, second, on the status of the vegetation that grows on it.

b. Using satellite data (reflectance in several bands of optical range of the electromagnetic spectrum) and topography attributes, we can estimate both the productivity of the site and the vegetation status in an integrated manner. Then we can estimate the spatial variation of biomass concentrations. Using terrain data, the variation is scaled to the actual values for specific areas and subsequently aggregated at any available administrative division (stands, sites or districts).
In order to apply this approach in the estimation of AGB in any area the following steps should be done:

a. Selection of the geographic area: It is first necessary to define the limits of the study area and the stands of interest. One may not be able to divide into stands if one does not have enough previous information and the results can be aggregated in the proper spatial division later (see step f).

b. Gathering and processing satellite images: The images used should be subject to the following treatments:
i. Eliminate the presence of clouds and systematic errors. In the case of Landsat ETM + error must be corrected SLC-off explicitly.
ii. Geometric correction for integration into GIS environment.
iii. Radiometric correction to reduce topographic and atmospheric errors.
iv. Calculation of vegetation indexes and Tasseled Cap components.
c. Collection of field data: Field data can be collected especially for AGB estimation or can be available from previous inventories. Data should be expressed in biomass per unit area (i.e. hectare) and associated with a point in geographical formal space (i.e., UTM coordinates). Whatever the case, the field estimations of biomass can be made in any of the following cases:
i. If data are available at the individual tree, apply allometric equations by species.
ii. If data are aggregated for each plot, apply biomass functions.
d. Data checking and cleaning: To perform the geostatistical analysis, it is necessary to create integrated data tables that incorporate both the biomass data, obtained from field data, plus all available covariates (satellite and topographical). The data should be reviewed, validated, and one should eliminate those displaying an aberrant behavior.
e. Geostatistical modeling: Using the data structure obtained in step d, perform geostatistical analysis including the following sub-steps:
i. Analysis of multivariate spatial correlation (variogram analysis) to obtain experimental direct and cross variograms and to fit variogram models required for interpolation.
ii. Obtain local estimations of biomass and levels of uncertainty (estimation error variances) via cokriging throughout the study area.
iii. Masking for estimating administrative units or stands of interest. To get accurate estimates, it is important to rule out areas with no vegetation.
f. Report results and prepare associated maps.

In the previous paragraphs, one of the most important steps is the collection of field data. These data allow modeling the autocorrelation of biomass in space and its cross-correlation with satellite and topographic variables. When these data are available, the procedure for the estimation should be the one already described. However, sometimes no data are available or they cannot be collected on time or the costs are not reasonable. In this case, one may use known variogram models to make a "blind" estimation using a slightly alternative method: simple cokriging, which assumes that the average biomass is known. We propose that this average can be obtained using the forest growth simulators that are available in many countries, e.g., Radiata and Eucasim growing models and software in Chile.

5. Conclusions

The use of covariates extracted from SRTM elevation model and LANDSAT images allows for estimates with a greater level of detail than those obtained by using only data field. This can be corroborated by comparing the estimates by cokriging with those that would be obtained with univariate kriging. We hypothesize that the set of covariates accounts, through their spatial dependence, for two fundamental aspects to explain existing biomass:
a. The quality of the forest site. Topographic variables (altitude, slope and orientation) inform in a synergistic way about the quality of the specific potential growing conditions (forest site).
b. Vegetation health and vigor are jointly captured by the vegetation indices and Tasseled Cap components.
The approach to this scale of work, using medium spatial resolution sensors, is to estimate AGB independently of species or plant community types and then overlap stands boundaries, or any other administrative division, to obtain the associated total AGB stocks. Coregionalization models (direct and cross variograms) are simplifications of reality; in particular, they may not detect anisotropies when having a too small amount of field data, allowing only for an omnidirectional inference. The number of field data should be such that the inference of AGB variogram is feasible, which is usually achieved with more than 100 data in each stratum. In order for this number to be reduced, we recommend the sampling of the area (site) to be as regular as possible, i.e. avoiding samples clustered in space.

In the future, we suggest identifying other covariates correlated with AGB, for example, an indicator of the amount of sunlight available or a local indicator of the ground geometry (concave, convex or plane) that is related to the availability of water. These indicators could be calculated from a digital elevation model, already available at several spatial resolutions.

6. Acknowledgment

We would like to express our thanks to Biocomsa Consortium, and therefore INNOVA CORFO CHILE, for funding most of the field work, data acquisition and processing. Also, we thank Miss Paz Acuña and Miss Lissette Cortés from GEP Lab. at Universidad de Chile, for their support in reviewing the text and for providing the reference cartography. Also we thank Helen Grover for proof reading the text.

7. References

Anuchin, N.P. (1960). Forest Mensuration. Second edition. Goslesbumizdat. Moskova-Leningrado.454 pp

Ardo, J. (1992). Volume quantification of coniferous forest compartments using spectral radiance record by LANDSAT Thematic Mapper. *International Journal of Remote Sensing*, 13, 1779-1786

Ares & Braener (2005). Above ground biomass partitioning in loblolly pine silvopastoral stands: Spatial configuration and pruning effects. *Forest Ecology and Management* 219 (2005) 176-184

Avery, Th. & Burkhart, H. (1994). Forest Measurements. Fourth edition. McGraw-Hill. ISBN 0-07-002556-8. 408 pp

Baffetta, F.; Fattorini, L.; Franceschi, S. & Corona, P. (2009). Design-based approach to k-nearest neighbours technique for coupling field and remotely sensed data in forest surveys. *Remote Sensing of Environment*, 113(3):463-475

Baker, T.; Attiwill, P. & Stewart H. (1984). Biomass Equations for Pinus radiate in Gippsland, Victoria. New Zealand Journal of Forestry Science 14(1): 89-96

Bertini, R.; Chirici, G.; Corona, P. & Travadlini, D. (2007). Comparison between parametric and non-parametric methods for the spatialization of forest standing volume by integrating field measures, remote sensing data and ancillary data. *Forest@*, 4110–117:1082–1089

Birdsey R. (2004). Data gaps for monitoring forest carbon in the United States: An inventory perspective. Environmental Management 33 supplement 1, S1-S8.
Bitterlich, W. (1984). The Relascope Idea. Relative Measurements in Forestry. Commonwealth Agricultural Bureaux. ISBN 0-85198-539-4. 241 pp
Caldentey, J. (1989). Beziehungen zwischen Klimaelementen und der Produktivität von *Pinus radiata* Plantagen in Chile. Inaugural-Dissertation zur Erlangung der Doktorwürde der Forestwissenschaftlichen Fakultät der Ludwig-Maximilians-Universität München. 131 pp
Caldentey, J. (1995). Acumulación de biomasa en rodales naturales de *Nothofagus pumilio* en Tierra del Fuego, Chile. Investigación Agraria: Sistemas y Recursos Forestales 4(2): pp. 165-175
Chavez, P. (1996). Image-based atmospheric corrections - revisited and improved. *Photogrammetric Engineering & Remote Sensing*, Vol. 62, No. 9 (September 1996), pp. 1025-1036
Chilès, J.P. & Delfiner, P. (1999). *Geostatistics: Modeling Spatial Uncertainty*, Wiley, New York.
CNE/GTZ/INFOR. (2008). Disponibilidad de residuos madereros. Residuos de la industria primaria de la madera – Disponibilidad para uso energético. Santiago, octubre 2007.54 pp
Cohen, W. & Spies, T. (1992). Estimating structural attributes of Douglas-fir/ western hemlock forest stands from LANDSAT and Spot imagery. *Remote Sensing of Environment*, 41 (1), 1–17
CONAF-CONAMA-BIRF. (1999). Catastro y evaluación de recursos vegetacionales nativos de Chile. Informe nacional con variables ambientales. Santiago. Chile. 90 pp
CORMA, (February 2011). Available from http://www.corma.cl/corma_info.asp
Coulston, J. (2008). Forest Inventory and Stratified Estimation: A Cautionary Note. Research Note SRS–16. Southern Research Station Forest Service. Department of Agriculture. United States. 6 pp
Curran, P.J.; Dungan, J. & Gholz, H. (1992). Seasonal LAI in slash pine estimated with LANDSAT TM. *Remote Sensing of Environment*, 39, 3–13
David, M. (1976). The Practice of Kriging, In: *Advanced Geostatistics in the Mining Industry*, M. Guarascio, M. David & C.J. Huijbregts, (Eds.), 31-48, Reidel, Dordrecht
Donoso, C. (1981). Tipos Forestales de los Bosques Nativos de Chile. Documento de Trabajo Nº. 38. Investigación y Desarrollo Forestal (CONAF, PNUD-FAO) (Publicación FAO Chile) 70 pp
Donoso, C., (1993). Bosques templados de Chile y Argentina. Variación estructura y dinámica. Ecología forestal. Ed. Universitaria. Santiago, Chile 484 pp
Donoso, S.; Peña-Rojas, K.; Delgado-Flores, C.; Riquelme, A. & Paratori, A. (2010). Above-ground biomass accumulation and growth in marginal *Nothofagus macrocarpa* forest in central Chile. Interciencia, 35(11):65-69
Eklundh, L.; Harrie, L. & Kuusk, A. (2001). Investigating relationships between LANDSAT ETM+ sensor data and leaf area index in a boreal conifer forest. *Remote Sensing of Environment*, 78, 229–251
Fazakas, Z.; Nilsson, M. & Olsson, H. (1999). Regional forest biomass and wood volume estimation using satellite data and ancillary data. *Agricultural and Forest Meteorology*, 98-99, pp. 417–425
FIA. (2001). Bosque nativo en Chile: situación actual y perspectivas. Fundación para la Innovación Agraria. Ministerio de Agricultura. ISBN 956-7874-14-X, Santiago, Chile. 111pp
Foody, G.; Boyd, D. & Cutler, M. (2003). Predictive relations of tropical forest biomass from LANDSAT TM data and their transferability between regions. Remote Sensing of Environment, 85, 463–474

Fournier, R. A.; Luther, J. E.; Guindon, L.; Lambert, M.C.; Piercey, D.; Hall, R.J. & Wulder, M.A. 2003, Mapping above-ground tree biomass at the stand level from inventory information: test cases in Newfoundland and Québec. Canadian Journal of Forest Research 2003, 33, 1846-1863.

Franklin, J. (1986). Thematic Mapper analysis of coniferous forest structure and composition. International Journal of Remote Sensing, 7 (10), 1287–1301

Fuenzalida, H. (1965). Clima. Biogeografía. In: Geografía Económica de Chile, Texto refundido: pp. 98-152; 228-67. CORFO

Fundación Chile. (2005). Tablas Auxiliares de Producción. Simulador de Árbol Individual para Pino Radiata (Pinus radiata D. Don): Arquitectura de Copa y Calidad de Madera. 100pp

Gajardo, R. (1994). La Vegetación Natural de Chile. Clasificación y Distribución Geográfica. Editorial Universitaria, Santiago, Chile. 165 pp

Garfías, R. (1994). Crecimiento y biomasa en renoval raleado de Nothofagus alpina (Poepp, et Endl) Oerst, en la provincia de Bio-Bio, VIII Region. Tesis Ingeniería Forestal. Universidad Chile. Facultad de Ciencias Forestales y conservación de la naturaleza. Santiago, Chile. 64pp

Gayoso, J.; Guerra, J. & Alarcón, D. (2002). Contenido de carbono y funciones de biomasa en especies nativas y exóticas. Proyecto FONDEF D98I1076 Medición de la capacidad de captura de carbono en bosques de Chile y promoción en el mercado mundial. 157 pp

Gemmell, F. (1995). Effects of forest cover, terrain, and scale on timber volume estimation with Thematic Mapper data in the rocky mountain site. Remote Sensing of Environment, 51, 291–305

Gerding, V. (1991). Manejo de las plantaciones de Pinus radiata D. Don en Chile. BOSQUE 12(2):3-10

Gilabert, H.; Meza, F.; Cabello, H. & Aurtenenchea, M. (2010). Estimación del carbono capturado en las plantaciones de pino radiata y eucaliptos relacionados con el DL 701 de 1974. Informe final. Oficina de Estudios y Políticas Agrarias. ODEPA. Ministerio de Agricultura. Gobierno de Chile.

Goulard, M. & Voltz, M. (1992). Linear Coregionalization Model: Tools for Estimation and Choice of Cross-Variogram Matrix. Mathematical Geology, Vol.24, No.3, pp. 269-286

Gringarten, E. & Deutsch, C.V. (2001). Variogram Interpretation and Modeling, Mathematical Geology, Vol.33, No.4, pp. 507-534

Hall, R.; Skakun, R.; Arsenault, E. & Case, B. (2006). Modeling forest stand structure attributes using LANDSAT ETM+ data: Application to mapping of above ground biomass and stand volume. Forest Ecology and Management, 225, 378–390

Herrera, S.&Waisberg, R. (2002). Estimación de carbono almacenado en el Tipo Forestal Roble-Raulí–Coigüe (Nothofagus obliqua-Nothofagus alpina–Nothofagus dombeyi), para determinar los beneficios ambientales de someterlo a sumidero. Memoria de título Ingeniería de Ejecución en ambiente. Departamento de Ingeniería Geográfica, Facultad de Ingeniería, Universidad de Santiago de Chile.
Horler, D. & Ahern, F. (1986). Forestry information content of Thematic Mapper data. *International Journal of Remote Sensing*, 7, 405–428

Husch, B.; Miller, C. & Beers, T. (1993). Forest Mensuration. Krieger Publishing Company, Third Edition. ISBN 0-89464-821-7, Malabar, Florida. 402 pp

INFOR. (2010). Wisdom, Plataforma de Información de la Oferta de Dendrocombustibles en Chile, In: Seminario Centro de Energías Renovables “Energía sustentable de la biomasa: oportunidades y desafíos”

Isaaks, E.H. & Srivastava, R.M. (1989). *An Introduction to Applied Geostatistics*, Oxford University Press, New York

Ishii, T. & Tateda, Y. (2004). Leaf Area Index and Biomass Estimation for Mangrove Plantation in Thailand. In: Geoscience and Remote Sensing Symposium, 2004. IGARSS ’04. Proceedings. 2004 IEEE International, 20-24 Sept. 2004. Vol 4: 2323 – 2326

Jakubauskas, M. & Price, K. (1997). Empirical relationships between structural and spectral factors of Yellowstone lodgepole pine forests. *Photogrammetric Engineering and Remote Sensing*, 63 (12), 1375–1381

Keith, H.; Barret, D. & Keenan, R. (2000). Review of Allometric Relationships for Estimating Woody Biomass for New South Wales, the Australian Capital Territory, Victoria, Tasmania and South Australia. National Carbon Accounting System Technical Report N° 5B. Australian Greenhouse Office 121 pp.

Ketterings, Q.; Coe, R.; van Noordwijk M.; Ambagau, Y. & Pal, Ch. A. (2001). Reducing uncertainty in the use of allometric biomass equations for predicting above-ground tree biomass in mixed secondary forests. *Forest Ecology and Management* 146: 199-2009

Kimes, D.; Holben, B.; Nickeson, J. & Mckee, W. (1996). Extracting forest ages in a pacific northwest forest from Thematic Mapper and topographic data. *Remote Sensing of Environment*, 56, 133–140

Koch, B. & Dees, M. (2008). Forestry applications. In: Advances in Photogrammetry, Remote Sensing and Spatial Information Sciences: 2008 ISPRS Congress Book, Chapter 32 - Li, Chen & Baltsavias (eds). Taylor & Francis Group, London. pp 439-465.

Labrecque, S.; Fournier, R.; Luther, J. & Piercy, D. (2006). A comparison of four methods to maps biomass from LANDSAT–TM and inventory data in western Newfoundland. *Forest Ecology and Management*, 226, 129–144

Lathrop, R. & Pierce, L. (1991). Ground-based canopy transmittance and satellite remotely sensed measurements for estimation of coniferous forest canopy structure. *Remote Sensing of Environment*, 36, 179–188

Lavery, P. (1986). Plantation Forestry with Pinus radiata. Review Paper N° 12. School of Forestry. University of Canterbury, Christchurch, New Zealand 255 pp

Lewis N. & Ferguson, I. (1993) in association with Sutton, W.; Donald, D. & Lisboa, H. Management of radiata Pine.ISBN 0-909605-79-3 Langley Editing, Melbourne, Australia 404 pp

Leyton, J. (2009). Tenencia Forestal en Chile. Available from http://www.fao.org/forestry/17192-0422df95bf58b971d853874bb7c5755f7.pdf

Loetsch, F., Zoehrer, F. & Haller, K.E. (1973). *Forest Inventory. Vol. 2* B.L.V. Verlagsgesellschaft. München. 469 pp
Lu, D. (2005). Aboveground biomass estimation using LANDSAT TM data in the Brazilian Amazon Basin. *International Journal of Remote Sensing*, 26, 2509–2525

Lu, D.; Mausel, P.; Brondizio, E. & Moran, E. (2004). Relationships between forest stand parameters and LANDSAT Thematic Mapper spectral responses in the Brazilian Amazon basin. *Forest Ecology and Management*, 198, 149–167

Luebert, F. & Pliscoff, P. (2006). Sinopsis bioclimática y vegetacional de Chile. Santiago de Chile, Editorial Universitaria. ISBN 956-11-1832-7, 316 pp

Madgwick, H. (1994). *Pinus radiata* – Biomasa, Form and Growth. H.A.I. Madwick (Ed) ISBN 0-473-02375-X, Rotorua New Zealand. 428pp

Maselli, F.; Chirici, G.; Bottai, L.; Corona, P. & Marchetti, M. (2005). Estimation of Mediterranean forest attributes by the application of k-NN procedure to multitemporal LANDSAT ETM+ images. *International Journal of Remote Sensing*, 17:3781–3796

McRoberts R. & Tomppo, E. (2007). Remote sensing support for national forest inventories. *Remote Sensing of Environment*, 110:412–419

McRoberts R.; Tomppo, E.; Finley, A. & Heikkinen, J. (2007). Estimating areal means and variances of forest attributes using the k-Nearest Neighbors technique and satellite imagery. *Methods*, 111:466 - 480

Mickler, R.; Earnhardt, T. & Moore, J. (2002). Regional estimation of current and future forest biomass. *Environmental Pollution*, 116, S7–S16

Morales, R.; Weintraub, A.; Peters, R. & García, J. (1979). Modelos de simulación y manejo para plantaciones forestales. FO: DP/CHI/76/003. Documento de trabajo N° 36. Santiago de Chile. 155pp

Nelson, R.F., Kimes, D.S., Salas, W.A. & Routhier, M. (2000). Secondary forest age and tropical forest biomass estimation using Thematic Mapper imagery. Bioscience, 50, pp. 419–431.

Peña, M. (2007). Correcciones de una imagen satelital ASTER para estimar parámetros vegetacionales en la cuenca del río Mirta, Aysén. Bosque 28(2): 162-172p.

Peterson, D.; Spanner, M.; Running, S. & Teuber, K. (1987). Relationship of Thematic Mapper simulator data to leaf area index of temperate coniferous forests. *Remote Sensing of Environment*, 22, 323–331

Peterson, D.; Westman, W.; Stephenson, N.; Ambrosia, V.; Brass, J. & Spanner, M. (1986). Analysis of forest structure using Thematic Mapper simulator data. *IEEE Transactions in Geoscience and Remote Sensing*, 24, 113–121

Phua, M. & Saito, H. (2003). Estimation of biomass of a mountainous tropical forest using LANDSAT TM data. *Canadian Journal of Remote Sensing*, 29, 429–440

Prodan, M.; Peters, R.; Cox, F. & Real, P. (1997). Mensura Forestal. Serie Investigación y Educación en Desarrollo Sostenible. IICA BMZ/gtz

Riaño, D.; Chivieco, E.; Salas, J. & Aguado, I. 2003. Assessment of Different Topographic Corrections in Landsat-TM Data for Mapping Vegetation Types. *IEEE Transactions in Geoscience and Remote Sensing*, vol. 41(5): 1056:1061

Rivoirard, J. (1987). Two Key Parameters When Choosing the Kriging Neighborhood, *Mathematical Geology*, Vol.19, No.8, pp. 851-856

Rivoirard, J. (2004). On Some Simplifications of Cokriging Neighborhood, *Mathematical Geology*, Vol.36, No.8, pp. 899-915
Roy, P. & Ravan, S. (1996). Biomass estimation using satellite remote sensing data: an investigation on possible approaches for natural forest. *Journal of Bioscience*, 21 (4), 535–561

Saez, M. (1991). Biomasa y contenido de nutrientes e renovales no intervenidos de roble-rauíl (*Nothofagus obliqua* (mirb) Oerst. – *Nothofagus alpina* (Poepp. et Ende.) Oerst.) en suelos volcánicos de la precordillera andina, IX Región. Memoria de título Ingeniería Forestal. Facultad de Ciencias Forestales. Universidad de Chile. 96 pp

Schlatter, J. & Gerding, V. (1984): Important site factors for *Pinus radiata* growth in Chile. In: Grey, D.C., Schonau, A.P.G., Schutz, C.J. & Van Laar, A. (Editors). Symposium on Site and Productivity of Fast Growing Plantations, Pretoria and Pietermaritzburg, South Africa 30 April 11- May 1984 pp 541-549

Schlatter, J. (1977). *La Relación entre suelo y Plantaciones de Pinus radiata* D.DON en Chile Central Análisis de la Situación Actual y Planteamientos para su Futuro Manejo. Bosque Vol. 2 Nº 1 31 pp

Schlegel, B. (2001). Estimación de la biomasa y carbono en bosques del tipo forestal siempreverde. Simposio internacional medición y monitoreo de la captura de carbono en ecosistemas forestales. 18-20 Octubre 2001. Valdivia, Chile. 13 pp

Schmidt, A.; Poulain, M.; Klein, D.; Krause, K.; Peña-Rojas, K.; Schmidt, H. & Schulte, A. (2009). Allometric above-belowground biomass equations for *Nothofagus pumilio* natural regeneration in the Chilean Patagonia. Ann. For. Sci. 66 (5):315-323.

Stein, M.L. (2002). The Screening Effect in Kriging, *Annals of Statistics*, Vol.30, No.1, pp. 298-323

Steininger, M. (2000). Satellite estimation of tropical secondary forest above-ground biomass: data from Brazil and Bolivia. Int. J. Remote Sensing Vol 21 Nº 6 & 7, 1139 – 1157

Subramanyam, A. & Pandalai, H.S. (2008). Data Configurations and the Cokriging System: Simplification by Screen Effects, *Mathematical Geosciences*, Vol.40, No.4, pp. 425-443

Thessler, S.; Sesnie, S. & Rambosendana, Z. (2008). Using k-NN and discriminant analyses to classify rain forest types in a LANDSAT TM image over northern Costa Rica. *Remote Sensing of Environment*, 112(5):2485-2494

Tomppo, E. & Halme, M. 2004. Using coarse scale forest variables as ancillary information and weighting of variables in k-NN estimation: A genetic algorithm approach. *Remote Sensing of Environment*, 92:1–20

Tomppo, E.; Gagliano, C.; Denatale, F.; Katila, M. & McRoberts, R. (2009). Predicting categorical forest variables using an improved k-Nearest Neighbour estimator and LANDSAT imagery. *Remote Sensing of Environment*, 113(3):500-517

Toro, J. & Gessel, S. (1999). Radiata pine plantations in Chile. New Forests 18: 33–44

Trotter, C.; Dymond, J. & Goulding, C. (1997). Estimation of timber volume in a coniferous plantation forest using LANDSAT TM. *International Journal of Remote Sensing*, 18, 2209–2223

Tucker, C. (1979). Red and photographic infrared linear combinations for monitoring vegetation. *Remote Sensing of Environment*, 8: 127-150

Turner, D.; Cohen, W.; Kennedy, R.; Fassnacht, K. & Briggs, J. (1999). Relationships between leaf area index and LANDSAT TM spectral vegetation indices across three temperate zone sites. *Remote Sensing of Environment*, 70, 52–68
Valdez R, M.; González & De Los Santos, H. M. (2006). Estimación de cobertura arbórea mediante imágenes Satelitales multiespectrales de alta resolución. Agrociencia 40(3): 383-394 p. ISSN 1405-3195.

Wackernagel, H. (2003). Multivariate Geostatistics: an Introduction With Applications, Third Edition, Springer, Berlin

Wackernagel, H.; Bertino, L.; Sierra, J.P. & González del Río, J. (2002). Multivariate Kriging for Interpolating With Data From Different Sources, In: Quantitative Methods for Current Environmental Issues, C.W. Anderson, V. Barnett, P. Chatwin & A.H. El Shaarawi, (Eds.), 57-75, Springer-Verlag, London

Wang, Ch. (2006). Biomass allometric equations for 10 co-occurring tree species in Chinese temperate forests. Forest Ecology and Management 222 (2006) 9-16

Wulder, M. (1998). Optical remote-sensing techniques for the assessment of forest inventory and biophysical parameters. Progress in Physical Geography, 22, pp. 449-476.

Zewdie, M.; Olsson, M. & Verwijst, Th. (2009). Above-ground biomass production and allometric relations of Eucalyptus globulus Labill. coppice plantations along a chronosequence in the central highlands of Ethiopia. Biomass and Bioenergy 33 (2009) 421-428

Zheng, D.; Heath, L.S. & Ducey, M.J. (2007). Forest biomass estimated from MODIS and FIA data in the Lake States: MN, WI, and MI, USA. Forestry 2007, 80, 265-278.

Zheng, D.; Rademacher, J.; Chen, J.; Crow, T.; Bresee, M.; Le Moine, J. & Ryu, S. (2004). Estimating aboveground biomass using LANDSAT 7 ETM+ data across a managed landscape in northern Wisconsin, USA. Remote Sensing of Environment, 93, 402-411
The accurate measurement of ecosystem biomass is of great importance in scientific, resource management and energy sectors. In particular, biomass is a direct measurement of carbon storage within an ecosystem and of great importance for carbon cycle science and carbon emission mitigation. Remote Sensing is the most accurate tool for global biomass measurements because of the ability to measure large areas. Current biomass estimates are derived primarily from ground-based samples, as compiled and reported in inventories and ecosystem samples. By using remote sensing technologies, we are able to scale up the sample values and supply wall to wall mapping of biomass. Three separate remote sensing technologies are available today to measure ecosystem biomass: passive optical, radar, and lidar. There are many measurement methodologies that range from the application driven to the most technologically cutting-edge. The goal of this book is to address the newest developments in biomass measurements, sensor development, field measurements and modeling. The chapters in this book are separated into five main sections.

How to reference
In order to correctly reference this scholarly work, feel free to copy and paste the following:

Jaime Hernández, Patricio Corvalán, Xavier Emery, Karen Peña and Sergio Donoso (2012). Geostatistical Estimation of Biomass Stock in Chilean Native Forests and Plantations, Remote Sensing of Biomass - Principles and Applications, Dr. Lola Fatoyinbo (Ed.), ISBN: 978-953-51-0313-4, InTech, Available from: http://www.intechopen.com/books/remote-sensing-of-biomass-principles-and-applications/geostatistical-estimation-of-biomass-stock-in-chilean-native-forests-and-plantations
