High-resolution VLA Imaging of Obscured Quasars: Young Radio Jets Caught in a Dense ISM

Pallavi Patil1,2,16, Kristina Nyland3, Mark Whittle1, Carol Lonsdale2, Mark Lacy2, Colin Lonsdale4, Dipanjan Mukherjee5,6,7, A. C. Trapp8, Amy E Kimball9, Lauranne Lanz10,11, Belinda J. Wilkes12, Andrew Blain13,14, Andreas Efstathiou15,16, and Catherine Vlahakis17

1 Department of Astronomy, University of Virginia, 530 McCormick Road, Charlottesville, VA 22903, USA; pp3uq@virginia.edu
2 National Radio Astronomy Observatory, 520 Edgemont Road, Charlottesville, VA 22903, USA
3 National Research Council, resident at the Naval Research Laboratory, Washington, DC 20375, USA
4 Massachusetts Institute of Technology, Haystack Observatory, Westford, MA 01886, USA
5 Inter-University Centre for Astronomy and Astrophysics, Post Bag 4, Ganeshkhind, Pune—411007, India
6 Dipartimento di Fisica Generale, Universita degli Studi di Torino, Via Pietro Giuria 1, I-10125 Torino, Italy
7 INAF, Osservatorio Astrofisico di Torino, Strada Osservatorio 20, I-10025 Pino Torinese, Italy
8 Department of Physics and Astronomy, University of California Los Angeles, CA 90095-1562, USA
9 National Radio Astronomy Observatory, 1003 Lopezville Rd., Socorro, NM 87801, USA
10 Department of Physics and Astronomy, Dartmouth College, 6127 Wilder Laboratory, Hanover, NH 03755, USA
11 Department of Physics, The College of New Jersey, 2000 Pennington Road, Ewing, NJ 08628, USA
12 Center for Astrophysics, Harvard & Smithsonian, Cambridge, MA 02138, USA
13 Department of Physics & Astronomy, University of Leicester, University Road, Leicester LE1 7RH, UK
14 Centre for Astrophysics Research, School of Physics, Astronomy and Mathematics, University of Hertfordshire, College Lane, Hatfield AL10 9AB, UK
15 School of Sciences, European University Cyprus, Diogenis Street, Engomi, 1516, Nicosia, Cyprus

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Abstract

We present new subarcsecond-resolution Karl G. Jansky Very Large Array (VLA) imaging at 10 GHz of 155 ultraluminous (L_{bol} ~ \sim 10^{11.7} - 10^{14.2} L_{\odot}) and heavily obscured quasars with redshifts z ~ 0.4–3. The sample was selected to have extremely red mid-infrared–optical color ratios based on data from the Wide-Field Infrared Survey Explorer (WISE) along with a detection of bright, unresolved radio emission from the NRAO VLA Sky Survey (NVSS) or Faint Images of the Radio Sky at Twenty cm Survey. Our high-resolution VLA observations have revealed that the majority of the sources in our sample (93 out of 155) are compact on angular scales \sim 0.2” (<1.7 kpc at z ~ 2). The radio luminosities, linear extents, and lobe pressures of our sources are similar to young radio active galactic nuclei (e.g., gigahertz-peaked spectrum [GPS] and compact steep-spectrum [CSS] sources), but their space density is considerably lower. Application of a simple adiabatic lobe expansion model suggests relatively young dynamical ages (~10^{4–7} yr), relatively high ambient ISM densities (~1–10^4 cm^{-3}), and modest lobe expansion speeds (~30–10,000 km s^{-1}). Thus, we find our sources to be consistent with a population of newly triggered, young jets caught in a unique evolutionary stage in which they still reside within the dense gas reservoirs of their hosts. Based on their radio luminosity function and dynamical ages, we estimate that only \sim 20% of classical large-scale FR I/II radio galaxies could have evolved directly from these objects. We speculate that the WISE-NVSS sources might first become GPS or CSS sources, of which some might ultimately evolve into larger radio galaxies.

Unified Astronomy Thesaurus concepts: Active galaxies (17); Quasars (1319); Supermassive black holes (1663); Radio loud quasars (1349); Radio jets (1347); Radio telescopes (1360); Galaxy evolution (594)

Supporting material: figure set, machine-readable tables

1. Introduction

The active galactic nucleus (AGN) phenomenon, driven by accretion onto supermassive black holes (SMBHs), is believed to play an important role in the evolution of galaxies over cosmic time. There is now compelling evidence interlinking SMBH growth with host galaxy star formation and mass buildup. The primary evidence supporting SMBH–galaxy coevolution includes the empirical relation found between SMBH mass and the stellar velocity dispersion in galactic bulges (Kormendy & Ho 2013 and references therein) and the similarities in the cosmological evolution of AGN space densities and the star formation rate densities (Heckman & Best 2014; Madau & Dickinson 2014, and references therein).

The energy released by AGNs can have an impact on the surrounding interstellar medium (ISM) or circumgalactic medium via a variety of radiative and mechanical processes. Such interactions, often termed AGN feedback, can shock and/or expel the gas causing suppression or triggering of star formation in the host galaxy. Improving our understanding of SMBH–galaxy coevolution requires direct observations of AGN feedback in action during the peak epoch of stellar mass assembly and SMBH growth at 1 < z < 3. However, this phase of galaxy evolution is believed to take place in the presence of thick columns of gas and dust, leading to heavily obscured systems that are challenging to observe at optical and X-ray wavelengths (Hickox & Alexander 2018).

In dust-obscured systems, emission at optical, UV, and X-ray wavelengths from the AGN and/or nuclear starburst is absorbed by dust and reradiated in the infrared. Mid-infrared (MIR)
color diagnostics using infrared satellites such as the Spitzer Space Telescope (e.g., Lacy et al. 2004; Hatziminaoglou et al. 2005; Stern et al. 2005; Lacy et al. 2007, 2013; Donley et al. 2012), AKARI (e.g., Oyabu et al. 2011) and Wide-Field Infrared Survey Explorer (WISE; e.g., Mateos et al. 2012; Stern et al. 2012; Wu et al. 2012b; Assef et al. 2013; Lonsdale et al. 2015) have provided an effective means of identifying both obscured and unobscured AGN populations. Recent studies have suggested that the heavily reddened AGN population represents a transient phase of peak black hole fueling and stellar mass assembly (e.g., Eisenhardt et al. 2012; Wu et al. 2012a; Jones et al. 2014; Assef et al. 2015; Tsai et al. 2015; Díaz-Santos et al. 2016). The most extreme population of these galaxies, identified based on very red WISE colors, are called hot dust-obscured galaxies (Hot DOGs) owing to the presence of hot dust and high luminosity MIR emission (Eisenhardt et al. 2012; Wu et al. 2012a; Bridge et al. 2013).

One way to favor obscured AGN emission over obscured star formation is to additionally require a significant radio source. If the radio flux is greater than the MIR flux, the source is likely to be an AGN (e.g., Ibar et al. 2008). Thus, surveys that combine MIR and radio can identify obscured powerful jetted AGNs (e.g., Condon et al. 2002). Ideally, these sources will be similar to the Hot DOGs discussed above—they are AGNs caught at an early stage in their evolution—but with the additional possibility of showcasing jet-driven feedback.

Lonsdale et al. (2015) define such a sample, with an additional requirement that the optical counterparts are faint, which favors sources at intermediate redshift, $z \sim 1$–3. This sample forms the basis of the present study. As it stands, however, the Lonsdale et al. (2015) sample only made use of relatively low resolution radio observations. In the current paper, we present high-resolution X-band (8–12 GHz) Karl G. Jansky Very Large Array (VLA) images of this sample, which allow us to place much stronger constraints on the radio source properties. In particular, we wish to establish whether the sources are young, reside in a dense ISM, and may be caught in a state of expansion. In a companion paper (P. Patil et al. 2020, in preparation) we will use multifrequency observations to explore the radio spectral shapes, using these to further investigate the nature of the radio sources and the nature of the near-nuclear environments.

Section 2 summarizes the sample selection and the MIR properties of the sample. The VLA observations and data reduction are described in Section 3. We present source measurements and properties in Sections 4 and 5, respectively. We analyze our sample’s radio luminosity function in Section 6. Section 7 discusses how our sample might fit into an evolutionary framework with the other known classes of compact and extended radio sources. We also use an adiabatic expanding lobe model to derive some important source properties. Section 8 summarizes our conclusions. We adopt a ΛCDM cosmology with $H_0 = 67.7 \, \text{km s}^{-1} \, \text{Mpc}^{-1}$, $\Omega_\Lambda = 0.691$, and $\Omega_M = 0.307$ (Planck Collaboration et al. 2016).

2. Sample Selection

A detailed description of our sample selection is given in Lonsdale et al. (2015). Briefly, point sources from the WISE All-Sky catalog (Wright et al. 2010) with signal-to-noise ratio (S/N) $> 7$ in the 12 or 22 μm bands were cross-matched with sources from the National Radio Astronomy Observatory Very Large Array Sky Survey (NVSS; Condon et al. 1998) or, when available, the Faint Images of the Radio Sky at Twenty cm (FIRST; Becker et al. 1995) catalog. An important requirement was that the source be unresolved in the NVSS ($\theta_{\text{FWHM}} < 45^\prime$) and FIRST ($\theta_{\text{FWHM}} < 5^\prime$) catalogs in order to exclude sources dominated by large-scale, evolved radio emission. We also required the candidates to have relatively large radio-to-MIR flux ratios ($q_{22} = \log (J_{22 \mu m}/J_{20 \text{cm}}) < 0$), to favor AGN emission as opposed to star formation (Appleton et al. 2004; Ibar et al. 2008).

The selection also includes only objects with very red MIR colors, with a color cut defined by $(W1 - W2) + 1.25 \,(W2 - W3) > 7.17$ and a flux density cut of 7 mJy at 22 μm. Coupled with the limit on the $q_{22}$ parameter from above, this introduces a 1.4 GHz flux limit of about 7 mJy.

To minimize contamination by the non-AGN population, the sample excludes sources within 10° of the Galactic plane.

Each source was inspected using the Sloan Digital Sky Survey (SDSS; York et al. 2000) or Digitized Sky Survey (DSS; if not within the SDSS footprint), and only objects that were relatively optically faint or undetected were kept. We have not defined any specific optical selection criteria to favor sources within the required redshift interval and to not create a bias against large amounts of scattered optical light (Lonsdale et al. 2015). We also relied on follow-up spectroscopy to refine our sample by redshift. This ensures that the objects are likely to be at intermediate or high redshift, and given the extreme MIR to optical color, they are also likely to be heavily obscured. Given the intermediate or high redshift, the bright MIR fluxes then suggest high bolometric luminosity. A total of 167 sources met these selection criteria. We will discuss the completeness of the sample in Section 6.

2.1. Spectroscopic Redshifts

We obtained spectroscopic redshifts for 71 out of 80 attempted sources using several telescopes (see Lonsdale et al. 2015, for details). The remaining 9 sources were too faint to provide a reliable redshift. Figure 1 shows the redshift distribution, which is seen to be approximately flat from 0.5 < $z$ < 2 with a possible decline from 2 < $z$ < 2.8. The median value is $z_{\text{med}} \sim 1.53$. While the subset of sources targeted for redshift is likely biased to the optically brighter sources, it is unclear whether or not this translates to a bias in redshift—while optically brighter galaxies might be at lower redshift, optically brighter quasars might be at higher redshift. Taken at face value, our redshift distribution indicates that many of our sources lie close to the epoch of peak star formation and black hole fueling; some are nearer ($z \lesssim 1$) and may be suitable for detailed follow-up observations.

2.2. MIR and Submillimeter Properties

The 870 μm Atacama Large Millimeter/Submillimeter Array (ALMA) imaging of 49 sources (Lonsdale et al. 2015) and 850 μm James Clerk Maxwell Telescope (JCMT) Submillimetre Common-User Bolometer Array imaging of 30 sources (Jones et al. 2015) yielded 26/49 ALMA and 4/30 JCMT detections. Overall the MIR–submillimeter spectral energy distributions (SEDs) of our sample are likely to be dominated in the MIR by AGN-heated thermal dust emission. The selection of extremely red optical WISE colors and bright 22 μm emission revealed that these sources have high IR and

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17 We note that this infrared color selection criterion contained an error in Section 2 of Lonsdale et al. (2015). The error was a typo only and did not impact the analysis or any of the figures in Lonsdale et al. (2015). The color cut defined here is the correct version.
bolometric luminosities ($L_{\text{bol}} \sim 10^{11.7} - 10^{14.2} L_{\odot}$), with a few reaching the hyperluminous infrared galaxy regime. AGN populations identified using ultrared WISE color diagnostics are now known to belong to a class of IR-luminous obscured quasars such as Hot DOGs (e.g., Eisenhardt et al. 2012; Wu et al. 2012a; Assef et al. 2015). The MIR signatures and high-ionization lines in the spectra of our sample (Kim et al. 2013; E. Ferris et al. 2020, in preparation) are consistent with a population of radiative-mode obscured quasars. We refer our readers to Lonsdale et al. (2015) for more details on the MIR and submillimeter properties of our sample.

3. New VLA Data

3.1. Observing Strategy

We observed 167 sources from Lonsdale et al. (2015) at X band (8–12 GHz) with the VLA in the A- and B-arrays through projects 12B-127 and 12A-064, respectively. Due to the complexity of dynamic scheduling for such a large sample, 12 sources were not observed in any array, and 32 were observed in only one array. Therefore, the sample discussed in this paper consists of 155 sources, 26 of which lack imaging with the A-array and 6 of which lack imaging with the B-array. The A-array observations were divided into 13 separate scheduling blocks (SBs), and a total of 129 sources were observed between 2012 October and December. The B-array observations were divided into seven different SBs, and 149 sources were observed from 2012 June to August.

Sources closer to each other on the sky were scheduled in groups, with phase calibrators interleaved. However, to maximize observing efficiency, the same calibrator was not always reobserved after each target. This strategy was worth the inherent risk of failing to obtain phase closure for a few targets, because most of the sources were expected to be bright enough for self-calibration.

The observations took place during the Open Shared Risk Observing period when maximum bandwidths were limited to ~2 GHz. Our WIDAR correlator setup consisted of two basebands with central frequencies 8.6 and 11.4 GHz, respectively. The bandwidth of each baseband was 1024 MHz divided among eight 128 MHz wide spectral windows. The total bandwidth of our observations was 2 GHz. The correlator setup was kept identical for both of the arrays. Our observing strategy aimed to obtain snapshot imaging of the full sample with about 5 minutes of integration time per source with a theoretical rms noise level of about ~13 $\mu$Jy beam$^{-1}$.

3.2. Calibration and Imaging

We used the Common Astronomy Software Applications package (CASA; McMullin et al. 2007) version 4.7.0 for data editing, calibration, and imaging. The initial step was to remove bad data with the help of the VLA operators log, followed by visual inspection of the data in the uv-plane using the task PLOTMS. Hanning smoothing was performed prior to calibration to remove the rigging effect from the Gibbs phenomenon caused by strong radio frequency interference. The data were calibrated using the CASA VLA calibration pipeline (version 1.3.9).

We then used the pipeline weblog and test images of the targets and phase calibrators to examine the quality of the calibration. If necessary, additional flagging was done, followed by a rerun of the calibration pipeline. We then used the CASA task CLEAN to produce the final continuum image. Because of the wide bandwidths made available by the new correlator, we formed images using the multifrequency synthesis mode with two Taylor coefficients (by setting the CLEAN parameter nterms = 2) to more accurately model the spectral dependence of the sky. Also, to mitigate the effects of non-coplanar baselines during imaging, we used the W-projection algorithm with 128 w-planes. The FWHMs of the synthesized beam of the final images in the A- and B-arrays are typically $\theta_b \sim 0''2$ and $\sim 0''6$, respectively.

Despite our careful calibration and imaging strategy, a total of 13 targets (11 in A-array and 2 in B-array) suffered from severe phase closure issues. As a result, 110 sources have imaging in both arrays, 8 sources have only A-array imaging, and 37 sources have only B-array imaging. Thus, the analysis presented in the remainder of this paper is based on 155 sources.

4. Source Measurements

4.1. Fluxes

To determine source parameters such as peak flux density, integrated flux, deconvolved shape parameters, and all corresponding uncertainties, we used the JMFTF task available in the 31DEC18 version of the Astronomical Image Processing Software (AIPS). In most cases, the radio sources have either single- or multicomponent Gaussian-like morphologies, and their flux and shape parameters may be estimated by fitting one or more two-dimensional elliptical Gaussian models. For sources with extended, complex structures, we manually estimated the source parameters using the CASA Viewer.18

18 www.vla.nrao.edu/cgi-bin/oplogs.cgi
19 www.science.nrao.edu/facilities/vla/data-processing/pipeline
20 Following Nyland et al. (2016), we calculate flux measurement uncertainties as $\sqrt{N \times \sigma^2 + (0.03 \times S_{\text{int}})^2}$, where $N$ is the total number of synthesized beams over $3\sigma$ contour emission, $\sigma$ is the rms noise, and $S_{\text{int}}$ is the integrated flux of the region.
The flux measurement uncertainties were calculated by adding the error provided by JMFIT and the 3% VLA calibration error (Perley & Butler 2013) in quadrature. We provide the clean beam dimensions, peak flux, and total flux from our A- and B-array observations in Table C1.

The total flux distributions in A- and B-array observations span the ranges 0.18–45 mJy and 0.13–60 mJy, respectively, with similar medians of ~3.3 mJy. Figure 2 compares the integrated fluxes of the 110 sources with high-quality flux measurements from both A- and B-arrays. The designation “high-quality” here simply indicates no hint of image artifacts.

We find that, for most of our sample, the total flux measurements from each array are in good agreement. There are four sources that lie below the unity line in Figure 2 and have less flux recovered in the longer-baseline A-array observations. These sources may have a diffuse emission component that has not been recovered in the A-array data.21

There is also one outlier in Figure 2 with significantly higher flux in the B-array data compared to the A-array, possibly as a result of intrinsic source variability or calibration error.

4.2. Source Angular Sizes

We used the JMFIT task in AIPS to measure the angular sizes of our sources. For resolved sources, JMFIT22 requires that (1) the integrated flux be larger than the peak flux density and (2) the deconvolved major axis is greater than zero (within the relevant uncertainties). If neither of these criteria was satisfied, the source was classified as unresolved. The source-fitting algorithm gives a cautionary message when only one of two criteria is satisfied. We discuss our morphological classification in the next section, including our approach to sources with ambiguous JMFIT results.

Deconvolved source sizes were taken directly from JMFIT. The uncertainties were calculated based on the formalism given by Murphy et al. (2017):

\[
\frac{\sigma_\theta}{\theta_c} = \left[ 1 - \left( \frac{\theta_b}{\phi} \right)^2 \right]^{1/2},
\]

where \(\sigma_\theta\) and \(\sigma_\phi\) are the rms errors on the deconvolved (\(\theta\)) and measured (\(\phi\)) source sizes, respectively. The parameter \(\theta_b\) is the FWHM of the synthesized beam. For the unresolved sources, we consider the maximum deconvolved angular size provided by JMFIT to be an upper limit on the source size. For extended sources with non-Gaussian morphologies, we measured the angular sizes using the CASA Viewer. Table C2 provides the deconvolved source sizes and morphological classification. For sources with more than one component, separate measurements are given for each component.

4.3. Morphological Classification

As described in the previous section, the JMFIT task in AIPS uses two basic criteria to determine whether a source is formally resolved: the peak/total flux ratio and the deconvolved source size compared to the clean beam size. We use these criteria but modify the first to be more conservative by including a 3% uncertainty in the flux calibration (see Section 4.1).

We classify as “unresolved, U” sources that satisfy both criteria, deconvolved sizes consistent with zero in both axes and peak/total flux ratio of unity within the uncertainties. We classify as “slightly resolved” sources that show finite size along one of the two axes and a peak/total flux ratio consistent with 1. We classify as “resolved, R” sources that show finite size along both axes and a peak/total flux ratio less than 1 (within 1\(\sigma\), following Owen 2018). Sources with more than a single distinct component are classified as double-, triple-, or multicomponent morphologies. Figure 3 shows the distribution of morphologies in our sample. We note that the entire analysis is performed separately for the A- and B-array data, and when possible, A-array results are preferred for the morphological classification and further analysis. In summary, we categorize our sample sources into the following morphological classes:

1. Unresolved (UR): The source is unresolved along both the major and minor axes, and the peak/total flux ratio is unity within the 1\(\sigma\) uncertainty.
2. Slightly resolved (SR): The source is unresolved along one of the axes, and the peak/total flux ratio is unity within the 1\(\sigma\) uncertainty.
3. Fully resolved (FR): The radio source is resolved along both the axes, and the peak/total flux ratio is <1.
4. Double (D): The source consists of two distinct components, each of which may be unresolved, slightly resolved, or fully resolved.
5. Triple (T): The source consists of three distinct components, resembling the core-jet or core-lobe emission seen in large-scale radio galaxies.
6. Multiple (M): The source consists of more than three distinct components.

Figure 3 shows the morphological classifications of the 155 sources in our final sample. Expressed as percentages, 55.5% ± 9.3% are unresolved, 13.5% ± 4.6% are slightly resolved,
The six morphological classes are UR (unresolved), SR (slightly resolved), R (resolved), D (double), T (triple), and M (multiple). Where available, A-array images are used, unless they were of poor quality. A total of 55.5% ± 9.3% of the sources are unresolved, with linear extents ≤ 1.7 kpc at z ∼ 2.

7.7% ± 3.5% are fully resolved single sources, 14.8% ± 4.8% are double sources, 6.4% ± 3.1% are triple sources, and 1.3% ± 1.4% are multicomponent sources. Figure 3 shows the distribution of angular sizes for each morphological class. There is a large span of source declinations and the use of both A- and B-array data. Deconvolved sizes are plotted for the slightly resolved sources, and outermost peak separation sizes are given for double, triple, and multiple sources.

4.4. In-band Spectral Indices

Our VLA X-band observations capture a wide range of frequencies, 8–12 GHz, offering the possibility of measuring “in-band” spectral indices, α (defined as $f_\nu \sim \nu^\alpha$). Although CASA generates a spectral index map with errors, we chose not to use it since its errors are calculated only as uncertainties to a polynomial fit and are less reliable at lower S/N (Cornwell et al. 2005; Rau & Cornwell 2011). Instead, we have chosen a more classical approach to estimate the in-band spectral index and its uncertainty. By dividing our bandwidth into two halves (centered at $\nu_1 = 8.6$ and $\nu_2 = 11.4$ GHz), we imaged each half separately using identical CLEAN parameters. We smoothed each 11.4 GHz image to match the resolution of the 8.6 GHz image using the task IMSMOOTH. We then reg ridded the smoothed 11.4 GHz image using the corresponding 8.6 GHz image as a template (using the CASA task IMREGRID) to ensure matched coordinate systems in the two images. Finally, we ran JMFIT to obtain source flux and shape measurements of all images.

The in-band spectral index was estimated using the following equation:

$$\alpha_{\text{in}} = \frac{\log_{10}(S_{\nu_1}/S_{\nu_2})}{\log_{10}(\nu_1/\nu_2)},$$  \hspace{1cm} (2)

where $\nu_1$ and $\nu_2$ are 11.4 and 8.6 GHz, respectively. Using standard propagation of errors, the uncertainty in the in-band spectral index is

$$\sigma_{\alpha_{\text{in}}} = \frac{\sqrt{[(\sigma_{S_{\nu_1}}/S_{\nu_1})^2 + (\sigma_{S_{\nu_2}}/S_{\nu_2})^2]}}{\log_{10}(\nu_1/\nu_2)} .$$  \hspace{1cm} (3)

The left panel in Figure 5 shows the resulting uncertainty, $\sigma_{\alpha_{\text{in}}}$, plotted against the average S/N of the 8.6 and 11.4 GHz images. As expected, lower S/N yields larger uncertainties in $\alpha_{\text{in}}$ with a threshold of S/N ≥ 70 for $\sigma_{\alpha_{\text{in}}} < 0.1$, which we take as a threshold of reliability for the calculated values of $\alpha_{\text{in}}$.

Condon (2015) gives a theoretical analysis of in-band spectral indices and their uncertainties that broadly confirms our simple approach above. Combining Equations (48) and (49) from Condon (2015) for an in-band spectral index $\alpha_{\text{in}}$ over a bandwidth of 8–12 GHz, we find

$$\sigma_{\alpha_{\text{in}}} \times \text{S/N} = \frac{\sqrt{12}}{\ln(\nu_{\text{max}}/\nu_{\text{min}})} \sim 8,$$  \hspace{1cm} (4)

where S/N is the signal-to-noise ratio of the source and $\nu_{\text{max}}$ and $\nu_{\text{min}}$ are the upper and lower ends of the observing bandwidth.
respectively. The middle panel of Figure 5 shows the product $\sigma_{\text{IB}} \times S/N$ for our data and broadly confirms this result, with values near 7–8 for a range of in-band spectral indices.

The right panel of Figure 5 shows the distribution of in-band spectral indices with values above/below our S/N threshold color-coded as orange/blue. The distribution is strongly peaked near the median value of $\alpha_{\text{IB}} = -1.0$, with 80% of the high-quality values within the range $-1.7$ to $-0.5$. We will discuss these spectral indices, together with the overall radio SEDs in a companion paper (P. Patil et al. 2020, in preparation). Briefly, the median spectral index is broadly consistent with optically thin synchrotron emission ($\alpha \sim -0.7$ near 1 GHz; e.g., Condon & Ransom 2016), perhaps steepened somewhat via radiative losses and inverse Compton scattering from either the cosmic microwave background or local infrared radiation fields. About 5% of our sources might plausibly have a flat spectrum (i.e., $\alpha > -0.5$), consistent with an unresolved synchrotron core. This is also consistent with the absence of evidence for short-timescale variability typical of beamed sources, indicated by the good overall agreement between the fluxes measured in our A- and B-configuration observations. We will address the spectral characteristics and the role of beamed core emission more thoroughly in the SED paper.

5. Source Properties

5.1. Diffuse Radio Emission?

Our sample was selected to have compact emission in the NVSS and FIRST catalogs. As discussed in Section 4, the majority of our sources have compact morphologies in our new high-resolution X-band observations. However, the presence of diffuse, extended emission on scales of a few arcseconds (which could be associated with earlier episodes of AGN activity) cannot be definitively ruled-out on the basis of the X-band data alone owing to surface brightness sensitivity limitations.

5.1.1. Constraints from Radio Surveys

To check on the incidence of such extended emission, we visually inspected images of all of our sources in NVSS and FIRST, as well as two additional wide-field radio surveys: the GMRT Sky Survey (TGSS; Intema et al. 2017) and the VLA Sky Survey (VLASS; Lacy et al. 2020). The observing frequency, angular resolution, maximum resolvable scale, and 1σ sensitivity for these surveys are summarized in Table 1, along with similar information for our X-band observations. The combination of our new X-band data with lower-resolution radio surveys provides a more complete picture of the radio morphologies of our sources, thus allowing us to constrain the presence of diffuse, extended emission.

We reconfirmed that all of our sources are indeed compact in NVSS. For the 51/155 sources included in the FIRST survey footprint, we inspected the FIRST images and found six sources that appear compact in NVSS but are either resolved into two distinct components or extended in FIRST. In all six of these cases, the multiple components identified in FIRST appear to be associated with radio AGN jets/lobes. We provide a further comparison of the NVSS and FIRST properties of our sources in terms of their fluxes in Section 5.1.2.

![Figure 5. Analysis of in-band spectral indices, $\alpha_{\text{IB}}$, and their errors, $\sigma_{\text{IB}}$. Left: relation between $\sigma_{\text{IB}}$ and the average S/N of the 8.6 and 11.4 GHz images, evaluated by simple propagation of errors. A threshold S/N of $\sim 70$ (vertical dashed line) ensures $\sigma_{\text{IB}} < 0.1$ (horizontal dashed–dotted line). Middle: the product $\sigma_{\text{IB}} \times S/N$ from our simple analysis confirms a theoretical analysis by Condon (2015) that predicts a value of $\sim 8$. Right: distribution of measured $\alpha_{\text{IB}}$ colored according to high S/N (>70; orange) or low S/N (<70; blue).](https://archive-new.nrao.edu/vlass/quicklook/)

Table 1

| Survey       | $\nu$ (GHz) | $\theta_{\text{arcsec}}$ | LAS (arcsec) | $\sigma_{\text{rms}}$ (mJy beam$^{-1}$) | $n_{\text{sources}}$ |
|--------------|-------------|--------------------------|--------------|----------------------------------------|----------------------|
| TGSS ADR1    | 0.15        | 25                       | 4104         | 3.5                                    | 152                  |
| NVSS         | 1.4         | 45                       | 970          | 0.45                                   | 155                  |
| FIRST        | 1.4         | 5                        | 36           | 0.15                                   | 51                   |
| VLASS        | 3           | 2.5                      | 58           | 0.12                                   | 153                  |
| X-band-B     | 10          | 0.6                      | 17           | 0.03                                   | 149                  |
| X-band-A     | 10          | 0.2                      | 5.3          | 0.03                                   | 129                  |

Note. Column (1): name of the radio survey. Column (2): frequency of the observation in GHz. Column (3): typical angular resolution of the survey in arcseconds. Column (4): largest resolvable angular scale in arcseconds. Column (5): 1σ rms noise in mJy beam$^{-1}$. Column (6): number of our sources observed in each survey.

We inspected the VLASS Epoch 1 “quicklook” images available at [https://archive-new.nrao.edu/vlass/quicklook/](https://archive-new.nrao.edu/vlass/quicklook/). We caution readers that these images are preliminary only—higher-quality survey products will be publicly available in the future, as discussed in Lacy et al. (2020).
TGSS, which provides a factor of two higher angular resolution than NVSS and a much lower frequency of 150 MHz, is more sensitive to steep-spectrum emission from older radio sources. We found a total of 15 sources with clearly resolved, extended emission and three sources with multiple components in TGSS. Finally, we examined the 3 GHz VLASS images of our sources, which have two times higher resolution than FIRST. We found 13 sources with extended morphologies and eight sources with multiple components.

Ultimately, the TGSS, FIRST, and/or VLASS images revealed extended or multicomponent emission in a total of 25/155 unique sources. Of these, 11 sources were not previously classified as being resolved in our X-band observations, thus leading to the reclassification of their morphologies. A summary of the properties of all sources with resolved emission identified in radio survey images is provided in Table E1, and image cutouts are shown in Figure E1. Thus, we conclude that the majority of our sources are indeed compact, even when observed at lower frequency and at lower resolution. We emphasize that the discovery of extended emission only has an impact on our study by modifying our morphological classification and possibly indicating a prior episode of activity. However, the presence of more extended emission does not affect our primary analysis of the more compact central radio source. It is these sources that we are most interested in because they are likely to be associated with the denser gas responsible for the high dust column and high MIR emission.

5.1.2. NVSS and FIRST Flux Ratios

As a further test for missed emission in our X-band observations, we compare in Figure 6 the 1.4 GHz NVSS and FIRST fluxes of our sources. Excluding six sources that are resolved in FIRST but not in NVSS (J1025+61, J1138+20, J1428+11, J1651+34, J2145−06, J2328−2), the fluxes are in good agreement above 30 mJy with slight (~5%) scatter to lower FIRST fluxes for weaker sources, with two outlier sources, J2322−00 and J1717+53, with flux ratios of 0.54 and 0.65, respectively. Neither of these sources shows any extended emission in TGSS, VLASS, or FIRST, and since both NVSS and FIRST were corrected for “CLEAN Bias,” it cannot explain the offsets. We note that other sources of bias exist for measurements at low S/N (e.g., Hopkins et al. 2015). Variability might explain some of the outliers (Mooley et al. 2016), though we emphasize that Figures 2 and 6 indicate that the majority of our sources are not likely to be variable on the timescales sampled by our data.

5.2. Physical Sizes

Figure 7 shows the distribution of physical source sizes, with the sample divided into resolved (including both slightly and fully resolved) and unresolved source morphologies. With the exception of 12 double or triple sources larger than 10 kpc, the rest are smaller than 5 kpc. Roughly 55% of the sources are unresolved with a median upper limit near 0.6 kpc. Given that our radio selection only requires sources to be compact on 40″ scales (NVSS, 100% of the sample) or 5″ scales (FIRST, 30% of the sample), we find that essentially all our sources are significantly more compact than these size limits, suggesting that our joint selection with luminous and red WISE MIR emission is preferentially associated with compact radio sources. A further check of whether the MIR selection is associated with compact radio emission is to ask whether an MIR blind radio survey with similar flux threshold and redshift range yields many compact sources.

Such a survey exists. The CENSORS sample of Best et al. (2003) used NVSS to select sources brighter than 7.8 mJy and cross-matched these with the ESO Imaging Survey (EIS). The resulting sample of 150 has similar median redshift and radio luminosity to our sample. However, the median radio source

![Figure 6. Ratio of fluxes measured in FIRST and NVSS as a function of NVSS flux. The black dotted line indicates a ratio of unity. For the majority of our sample, FIRST is able to recover most of the flux measured by NVSS. The gray shaded region shows the normalized median deviation ($\sigma_{\text{norm}} \sim 0.1$) of the flux ratio. Six sources with resolved morphologies in the FIRST are shown by the red symbols.](image)

![Figure 7. Linear sizes for the 71 sources with spectroscopic redshifts. We plot two separate histograms for the two broad morphological categories, resolved and unresolved. The blue histogram shows the largest linear extents for the resolved sources in our sample. The orange histogram with left-pointing arrows are the upper limits on the linear extents of unresolved sources and is stacked on top of the blue histogram.](image)
size for the CENSORS sample is 6", which is significantly larger than our own median source size of 0'.'1–0'.'2. Since the redshift distribution and flux cut for the two samples are similar, we conclude that the smaller source size of our sample is tied to the additional selection criteria of extreme MIR colors and luminosities.

Having established that our radio sources are compact, are there any previously established classes of radio sources that closely resemble our sources? Clearly they are different from the classical Fanaroff–Riley (FR) type I and II (Fanaroff & Riley 1974) radio sources, which are much more extended. Similarly, our sources, with their steep spectral index (Section 4.4), are also different from the compact flat-spectrum sources. There are four known classes of steep-spectrum radio sources that approximately match the angular and physical scales of our sample. These are the GPS (gigahertz-peaked spectrum; e.g., Fanti et al. 1990; O’Dea et al. 1991; Snellen et al. 1998; Fanti 2009; Collier et al. 2018), CSS (compact steep-spectrum; e.g., Peacock & Wall 1982; Spencer et al. 1989; Fanti et al. 1990, 2001; Sanghera et al. 1995), HFP (high-frequency peaker; e.g., Dallacasa et al. 2000; Stanghellini et al. 2009; Orienti & Dallacasa 2014), and FR0 classes (e.g., Sadler et al. 2014; Baldi et al. 2015). Of these, the FR0 class is significantly less luminous (<10^{24} W Hz^{-1}; Baldi et al. 2018), and while the available GPS/CSS samples are somewhat more luminous than our sample (see next section), an SED analysis (P. Patil et al. 2020, in preparation) confirms that a significant fraction of our sources have curved or peaked spectra in the GHz range, similar to the GPS/CSS sources. Thus, since our sample seems to share a number of properties with the GPS/CSS sources, we will use these as a point of comparison in the following discussion.

5.3. Radio Luminosities

Figure 8 presents the 1.4 GHz radio luminosity of our sample, which spans the range 25 ≤ log(L_{1.4 GHz}/W Hz^{-1}) ≤ 27.5, with a median of log(L_{1.4 GHz}/W Hz^{-1}) ≈ 26.3. We also use Figure 8 to compare with other well-known samples of radio AGNs to help place our own sample within a wider “zoo” of radio sources.

A representative sample of local (z < 0.3) radio AGNs was presented by Best & Heckman (2012), who cross-matched NVSS and FIRST sources with SDSS (radio luminosities calculated assuming a spectral index of −0.7). Clearly, our sample is roughly 2 dex more luminous than the local sample, confirming that our sample is much more luminous than the typical local radio AGN.

Next, we compare with the well-known low-frequency 3CRR survey, which is complete above S_{178 MHz} = 10.9 Jy (Laing et al. 1983). These span a wide range of redshift and luminosity and broadly divide into large-scale FR I and FR II radio sources (Fanaroff & Riley 1974). Our sample is, on average, 1.4 dex less luminous than the FR II galaxies and 1.3 dex more luminous than the FR I galaxies, though there is considerable overlap with both these samples.

Turning to radio sources that are, perhaps, better matched to the redshifts and physical scales of our own sources, the right side of Figure 8 includes samples of CSS and GPS sources (Spencer et al. 1989; Sanghera et al. 1995; O’Dea 1998; Fanti et al. 2001) and HFP sources (Dallacasa et al. 2000; Stanghellini et al. 2009). These samples show considerable overlap, though the median luminosities of the CSS, GPS, and HFP samples are larger by ~1, 1.8, and 0.5 dex, respectively.
Overall, then, while our sample is significantly more radio luminous than typical radio AGNs, it has intermediate luminosity when compared to samples of powerful radio-loud AGNs.

5.4. Radio Lobe Pressures

An important property of a radio source that affects how it develops is its internal pressure. To first order, the measured pressure likely reflects the pressure of the surrounding medium into which the radio source is expanding. If the radio source is overpressured relative to the surrounding medium, perhaps being fed by a nuclear jet, then the radio source will expand.

To estimate the internal lobe pressures in our sample sources, we use relations derived from synchrotron theory given in Moffet (1975) and Miley (1980):

$$P_l \approx \left(\frac{7}{9}\right)\left(\frac{B_{\text{min}}^2}{8\pi}\right),$$

where $P_l$ is the pressure in the lobe of a radio source in dyne cm$^{-2}$ and $B_{\text{min}}$ is the magnetic field in the magnetioionic plasma in G (gauss), derived using the common “minimum energy” or “equipartition” assumption that energy is shared approximately equally between the particles and the magnetic field. The equation for this magnetic field strength in G can be written as

$$B_{\text{min}} \approx 2.93 \times 10^{-4}\left[\frac{a}{f_{\nu}}\left(1+z\right)^{4-a}S_{\nu}X_{0.5}(\alpha)\right]^{1/7},$$

where the radio source has flux $S_{\nu}$ in Jy with spectral form $S_{\nu} \propto \nu^\alpha$ and angular size $\theta_\alpha \times \theta_\alpha$ arcsec, z is the redshift of the source, and $f_{\nu_2}$ is the comoving distance in Mpc. We choose the filling factor for the relativistic plasma, $f_{\nu_2}$, and the relative contribution of the ions to the energy, $a$, to be 1 and 2, respectively. The function $X_{0.5}(\alpha)$ handles integration over the frequency range from $\nu_1$ to $\nu_2$, where $\nu_1 = 0.01$ GHz and $\nu_2 = 100$ GHz, and is defined as

$$X_{\nu}(\alpha) = \left(\nu_2^{1+\alpha} - \nu_1^{1+\alpha}\right)/(q + \alpha),$$

where $q$ is 0.5 in this case and represents the spectral shape function of the synchrotron emission.

Knowledge of the source size is required, since it feeds directly into the estimate of source pressure. For resolved single, double, or triple sources we take the measured region sizes directly from JMFIT. For slightly resolved or unresolved sources we take a conservative approach and use the beam sizes directly from JMFIT. For slightly resolved or unresolved single, double, or triple sources we take the measured region directly into the estimate of source pressure. For resolved sources, the function $X_{\nu}(\alpha)$ handles integration over the frequency range from $\nu_1$ to $\nu_2$, where $\nu_1 = 0.01$ GHz and $\nu_2 = 100$ GHz, and is defined as

$$X_{\nu}(\alpha) = \left(\nu_2^{1+\alpha} - \nu_1^{1+\alpha}\right)/(q + \alpha),$$

where $q$ is 0.5 in this case and represents the spectral shape function of the synchrotron emission.

Knowledge of the source size is required, since it feeds directly into the estimate of source pressure. For resolved single, double, or triple sources we take the measured region sizes directly from JMFIT. For slightly resolved or unresolved sources we take a conservative approach and use the beam major axis as an upper limit to source size. This yields a conservative lower limit for the source pressure. Higher-resolution Very Long Baseline Array (VLBA) images for a number of the unresolved sources (P. Patil et al. 2020, in preparation) usually reveal even smaller-scale double lobes with yet higher pressures. Thus, our current treatment of the VLA images yields useful, though conservative, lower limits to the radio source pressures in the unresolved sources.

Figure 9 shows the distribution of pressures for our sample, with lower limits for the unresolved sources. For the resolved sources, the median pressure is \log(P_l/(\text{dyne cm}^2)) = -7.2 or log(P_l/(\text{cm}^3\text{K})) = +8.7. For the lower limits, these values are \log(P_l/(\text{dyne cm}^2)) = -6.3 or log(P_l/(\text{cm}^3\text{K})) = +9.5.

To help put our sample in context, we include the typical range of equipartition lobe pressures for a number of other classes of radio AGNs. On larger scales, the lobe pressures in FR I (e.g., Worrall & Birkinshaw 2000; Croston et al. 2008; Croston & Hardcastle 2014) and FR II (e.g., Croston et al. 2005; Harwood et al. 2016; Ineson et al. 2017; Vaddi et al. 2019) radio galaxies are roughly 3 dex lower than in our sample, almost certainly reflecting the much lower ambient pressures found on larger scales in the circumgalactic environment.

Figure 9 also shows the range of equipartition lobe pressures for CSS, GPS, and HFP sources taken directly from various studies (Mutel et al. 1985; Readhead et al. 1996; Orienti & Dallacasa 2014). There is a considerable overlap between our source pressures and those of the CSS, GPS, and HFP samples, possibly indicating a similarity in their properties and stage of development. However, a detailed comparison with these young radio AGNs is not straightforward because most measurements for the CSS, GPS, and HFP sources come from Very Long Baseline Interferometry observations with ~milliarcsecond-scale angular resolution capable of identifying much more compact radio structures. Indeed, preliminary analysis of our own VLBA follow-up survey shows that many of our unresolved sources also have more compact source components with significantly higher pressures (~1–3 dex; C. Lonsdale et al. 2020, in preparation). In all these comparisons, we have verified that our approach to measuring source pressures reproduces the source pressures given in these other papers.

The compact nature of the radio sources, together with their implied high pressures, seems to be a characteristic of the sample, and it is important to understand the origin of these high pressures. Unlike the lobes of extended FR I/FR II radio galaxies, the location of our radio sources deep within the host galaxy means that they are embedded within the relatively high-pressure environment of the central ~1 kpc region. If the radio sources are in fact overpressured relative to the ambient ISM, then that overpressure may generate an expansion that, when coupled to the small size, may indicate a young source. We will present a more quantitative analysis of the source pressures and ages in Section 7.2 when we use a simple model...
of jet-driven lobe expansion to fit the observed source sizes and pressures.

6. Radio Luminosity Function

The radio luminosity function (RLF) measures the number of radio sources per dex of radio continuum luminosity per comoving Mpc$^3$ (e.g., Condon et al. 2002). To calculate the RLF for our sample, we used the standard $1/V_{\text{max}}$ method (Schmidt 1968), which sums the space density for each source using a total volume within which that source could have been detected, given our sample selection criteria.

As described in Section 2, our sample selection is somewhat complicated and involves a combination of cuts in radio flux and source size, as well as infrared fluxes and colors. We therefore defined $V_{\text{max},i}$ for the $i$th source as

$$V_{\text{max},i} = \int_{z_{\text{min},i}}^{z_{\text{max},i}} \frac{dV_{i}}{dz} dz,$$

where $V_i$ is the comoving volume and $z_{\text{min},i}$ and $z_{\text{max},i}$ are the minimum and maximum redshift limits within which source $i$ would be included in our sample. The full redshift range searched was $z = 0–6$, with $\Delta z = 0.01$. To allow for the WISE color selection, we fitted a second-order fit to log $\nu$ versus log $F_\nu$ to the four measured WISE fluxes and used this SED to establish whether the source passed the color selection at each redshift. We did not include the radio source size criterion ($\theta < 45''$) since our observations indicate that none of our sources would be resolved by NVSS unless they were at a very low redshift ($z < 0.1$) with correspondingly small comoving volume. In practice, we find that shifting a source to higher redshift usually fails our selection owing to becoming too faint in the MIR. Similarly, we find that shifting a source to lower redshift usually fails our selection owing to the source becoming too blue in the MIR. The color selection is usually affected at lower redshift, where the $1/V_{\text{max}}$ factor is small, then the detailed form of the MIR SED does not have a significant impact on the final RLF. The luminosity function, $\phi$, is given by

$$\phi = \frac{4\pi N_{\text{tot}}}{\Omega N_i} \Delta \log L^{-1} \sum_i \frac{1}{V_{\text{max},i}},$$

where $\Omega$ is the solid angle of our survey, which is essentially that of the NVSS since the WISE survey is all-sky (a total area of 28,443 deg$^2$; Lonsdale et al. 2015), $\Delta \log L^{-1}$ is the width of each luminosity bin (with $L$ measured in units of W Hz$^{-1}$ here), and $N$ is the number of sources in each luminosity bin. Finally, the factor $N_{\text{tot}}/N_i$ corrects for the fact that we only measured redshifts for 46% of the total sample. A simple multiplicative factor is adequate since this subset is itself a significant fraction of the total and is relatively unbiased in redshift. The errors given are simply proportional to $\sqrt{N}$, boosted by $N_{\text{tot}}/N_i$.

Figure 10 shows the RLF of our sample, together with the RLFs of samples of high-excitation (radiative mode) and low-excitation (jet mode) radio-loud AGNs from Best et al. (2014). As expected given the deliberate selection of a rare class in color space, the RLF of our sample falls $\sim$2–3 dex below that of the radio AGNs from Best et al. (2014). However, this offset is likely to be a lower limit because the radio AGN sample has lower redshift ($0.5 < z < 1$). Given the well-known tendency for the comoving density of radio sources to increase with redshift (e.g., Best et al. 2014; Pracy et al. 2016; Ceraj et al. 2018), a more detailed comparison at matched redshift would likely find an even greater offset.

How should we interpret the lower space density of our sample compared to the other samples of radio AGNs? A straightforward explanation that supports our original motivation for selecting this sample is that the sources are in a short-lived phase (Lonsdale et al. 2015). Two qualities of the sample point to this: (a) they have compact, high-pressure radio sources, which can plausibly be argued are young, and (b) they have high bolometric luminosity but are optically faint, suggesting that the sample is dominated by obscured quasars with high columns. Within the fairly well-established theory of this class of object they are thought to be in a very young transient stage following a strong fueling event, probably associated with a merger (e.g., Hopkins & Hernquist 2006).

Another possible explanation for a low RLF is that the high-column material that yields both the red MIR colors and suppressed optical emission has a low covering factor due to a single cloud that happens to fall along our line of sight. However, we think that this is unlikely because another characteristic of our sample is that it has high MIR luminosity. First, a simple optically thick blackbody at $T \sim 60$ K must have a radius of $\sim 1$ kpc to generate such a high MIR luminosity. Second, the high MIR luminosity suggests that a large fraction of the AGN output is reprocessed by high-column absorbing material. Thus, the covering factor for the high-column material must be reasonably high.

7. Discussion

The overall scientific goal of our multiwavelength program is to identify heavily obscured quasars at the peak epoch of stellar mass assembly and SMBH growth and investigate their connection to galaxy evolution, possibly via the interaction of a powerful jet with the host’s ISM. Our unique selection criteria of extremely red WISE colors, along with compact radio and faint optical emission, promises to identify galaxies in a key stage of galaxy growth. In this section, we discuss the implications of our high-resolution radio imaging survey for the early phases of radio source evolution.
7.1. Radio Source Evolution

Several models have been proposed to describe the temporal evolution of the observed properties of radio sources, such as luminosity and spectral turnover frequency (e.g., Falle 1991; Fanti et al. 1995; Readhead et al. 1996; Kaiser & Alexander 1997; O’Dea & Baum 1997; Snellen et al. 2000; Kaiser & Best 2007; Kunert-Bajraszewska et al. 2010; An & Baan 2012; Maciel & Alexander 2014). Many of the early models assumed self-similar expansion of radio jets as they move first through dense ISM during their initial growth until they emerge into the IGM and ICM to become large-scale, old sources (Kaiser & Alexander 1997). Early semianalytic models found that the radio source luminosity increases as ram-pressure-confined lobes expand within the galaxy. The luminosity reaches a maximum when the jets pass the boundary of the ISM, and then it decreases as the lobes expand into the ICM to become FR I/FR II sources.

We now explore the evolutionary stage of our sample and its connection to the FR I/FR II population by plotting our sources on the radio power versus linear size (PD) diagram in Figure 11. The range of linear extents of our sources covers multiple classes of medium- and compact-scaled radio sources, including CSS and GPS populations. It is clear from Figure 11 and Section 5.3 that the radio luminosities of our sample sources lie between those of the classical FR I and FR II populations. We also show the two tracks given by An & Baan (2012) that follow the high radio power (dotted) and low radio power (dashed–dotted) sources. Our sources, being intermediate in luminosity, lie between these two tracks in Figure 11. The dashed line shows the boundary between stable and unstable jets in the model of An & Baan (2012). The fact that all except one (J2318–25) of our sources lie above this line is consistent with them having stable jets that yield small-scale edge-brightened double or triple morphologies, as indeed we find in the majority of the resolved sources.

Based on the evolutionary models given in An & Baan (2012) and following similar recent analyses (e.g., Jarvis et al. 2019), it seems that the position of our sources on the PD diagram relative to the jet instability criterion supports the possibility that they might eventually evolve into classical, FR I/II radio sources. This possibility is reinforced by the fact that our sources are heavily obscured, which points to a long-term fuel supply that could sustain the SMBH accretion for the ~100 Myr time span necessary to create larger radio sources. However, a more careful discussion of possible evolutionary links between the WISE-NVSS sources and classical radio galaxies must consider the source ages. This we now attempt using a simple jet lobe expansion model.

7.2. Lobe Expansion Model

There has been considerable work on models of radio source evolution in a variety of contexts, both analytic (e.g., Turner & Shabala 2015; Hardcastle 2018) and numerical (e.g., Mukherjee et al. 2016; Perucho 2019). Our sources may allow a relatively simple approach because the jets enter a dense, near-nuclear environment and are caught early in their development. While this may seem a potentially complex process, detailed simulations of just this situation (e.g., Mukherjee et al. 2016, 2018) suggest that the radio source develops in a quasi-spherical expansion, and in this case the analytic model of self-similar expansion is approximately correct.

A simple approach assumes purely adiabatic expansion, in which case the dynamics of the early phase of jet evolution can be approximated by the presence of a forward shock, a contact discontinuity, and an inner reverse shock. Following the mathematical treatment given in Weaver et al. (1977), a self-similar expansion of a spherical lobe can be expressed in terms

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**Figure 11.** 1.4 GHz spectral luminosity vs. largest linear source extent. Blue stars represent resolved sources, and orange arrows indicate unresolved sources from our sample. The colored boxes represent the parameter space occupied by different radio populations compiled by An & Baan (2012). The purple dotted and green dashed-dotted lines are the evolutionary tracks followed by high radio power (HRP) and low radio power (LRP) sources, respectively, based on the model given in An & Baan (2012). The vertical black dotted lines divide the entire plane into three broad size scales. The HFP, CSO, and GPS sources are on the compact scales (<1 kpc). CSS and a minority of FR I/FR II sources fall into the medium scales (~1–100 kpc), and FR I/II sources are the large-scale populations (>100 kpc). The black dashed line is the boundary between the stable and turbulent jet flows.
of our observed parameters\textsuperscript{24}

\begin{align}
    p_l &= 7.76 \times 10^{-10} F_{43} n_{\text{Myr}} R_l^{-3} \\
    p_t &= 1.17 \times 10^{-9} F_{43}^{2/3} n_{\text{v}}^{1/3} R_l^{-4/3} \\
    p_i &= 1.50 \times 10^{-12} F_{43} (V_l/c)^{-1} R_l^{-2},
\end{align}

where \( p_l \) is the pressure inside the lobe expressed in dyne cm\(^{-2} \), \( R_l \) is the radius of a lobe in kpc, \( F_{43} \) is the mechanical jet power in units of \( 10^{43} \) erg s\(^{-1} \), \( n_{\text{v}} \) is the ambient number density in cm\(^{-3} \), \( n_{\text{Myr}} \) is a dynamical age in Myr, \( V_l \) is the lobe velocity, and \( c \) is the velocity of light.

While Sections 5.2 and 5.4 describe our estimates of radio source size, \( R_l \), and pressure, \( p_l \), estimating the jet power, \( F_{43} \), is more uncertain. One approach is to assume that the jet power is related to the radio luminosity. While a number of studies have tried to establish such a link (e.g., Willott et al. 1999; Cavagnolo et al. 2010), others have argued that the relation is intrinsically quite scattered and has been amplified by selection bias (Godfrey & Shabala 2016). Bearing these caveats in mind, we cautiously adopt the relation given by Ineson et al. (2017):

\begin{equation}
    F_{43} = 5 \times 10^3 L_{151}^{0.89 \pm 0.09},
\end{equation}

where \( L_{151} \) is the rest-frame 151 MHz radio luminosity in units of \( 10^{28} \) W Hz\(^{-1} \) sr\(^{-1} \). For our sample, we estimate \( L_{151} \) using the 1.4 GHz luminosity from NVSS and a spectral index \( \alpha_{1.4} \) derived from the NVSS flux and our X-band flux. We exclude sources with flat/inverted indices (\( \alpha_{1.4} > -0.3 \)) and low-S/N sources with very steep indices (\( \alpha_{1.4} < -2.0 \)) since the uncertainty in the extrapolation to rest-frame \( L_{151} \) is large.

The left panel in Figure 12 shows the relation given in Equation (10) between source pressure, source size, and jet power, by plotting \( 3 \log R_l - \log F_{43} \) against \( \log p_l \) so that the source dynamical age, \( t_{\text{Myr}} \), appears as diagonal contours.

Using estimates for \( R_l \) and \( p_l \) from Sections 5.2 and 5.4 and \( L_{151} \) as described above, we find that the majority of our sources have dynamical ages in the range of \( 10^{5} \)–\( 10^{7} \) yr, with a median around 0.7 Myr. This is consistent with the overall picture that our sample contains young radio sources.

The middle panel of Figure 12 plots contours of external density, \( n_{\text{v}} \), and the distribution of points reveals relatively high densities, spanning \( 1\)–\( 10^7 \) cm\(^{-3} \), comparable to the higher-density phases in spiral disks or near-nuclear ISM. Again, this is consistent with our overall picture of a young radio source emerging into a dense medium. Most radio sources are within a kiloparsec of a galaxy center, where we expect high average gas density, especially given the steep optical–MIR SED colors pointing to high columns. Indeed, we can combine the inferred ambient gas density with our measured source size to estimate a column density. The majority span \( \log (N_{\text{H}}/\text{cm}^2) \sim 22–25 \), corresponding to \( A_V \sim 5–5000 \), which is consistent with the red optical–MIR SEDs and the identification of Compton-thick columns in the related Hot DOG population (e.g., Stern et al. 2014; Ricci et al. 2017).

The right panel in Figure 12 plots contours of lobe expansion speeds. It seems that the sources expand with modest, subluminal speeds \( V_l \sim 30–100000 \) km s\(^{-1} \) with a median near 450 km s\(^{-1} \). We note that our velocities are also similar to those found in much more detailed simulations of a similarly powered jet interacting with a dense clumpy medium (Mukherjee et al. 2016, 2018).

The discussion of the growth of compact radio sources is often framed as two contrasting possibilities: the small sizes result from youth or from “frustrated” jets that cannot expand owing to a dense surrounding medium (e.g., van Breugel et al. 1984; Bicknell et al. 2018). Our analysis suggests that both perspectives might be relevant for our sources—the sources are indeed young, but the ISM is also dense, and this slows the source expansion.

7.3. Prevalence of Gas-rich Mergers

Perhaps the most straightforward indication of youth would be to find a direct association with a short-lived phase in the host galaxy, such as a merger. Unfortunately, by selecting optically faint hosts (to avoid low-redshift sources), a simple inspection of the optical morphology is difficult. In the absence of direct observations, what might we expect? Despite early numerical simulations suggesting that luminous AGNs are

\textsuperscript{24} A complete derivation of these relations is given in Begelman (1999), as well as in Appendix A.
associated with gas-rich mergers (e.g., Hopkins et al. 2008), the observational evidence has been mixed. For example, Cisternas et al. (2011) and Villforth et al. (2017) fail to find the AGN–merger connection. However, when the AGNs are selected to be dusty and obscured, such as WISE AGNs, the association with mergers is much clearer, particularly at high luminosity (e.g., Satyapal et al. 2014; Weston et al. 2017; Goulding et al. 2018).

Recent numerical simulations of galaxy mergers also support this association. Blecha et al. (2018) have tracked the evolution of WISE colors and luminosities for gas-rich mergers, finding the closest match to our sample’s very red WISE colors during the brief final stage of coalescence.

Thus, our own sample of WISE-selected AGNs is very likely to contain a significant fraction of recent gas-rich mergers. Such a merger would be consistent with a newly triggered AGN with a radio jet.

7.4. Are WISE-NVSS Sources Truly Newborn?

Another approach that places the WISE-NVSS sources in a wider context is to use the RLF and dynamical age estimates to help establish a link to the other classes of radio source. First, the RLF analysis in Section 6 suggests that the WISE-NVSS sources have ~300 times lower space density than classical radio galaxies. Second, comparing the median dynamical age of \( \sim 10^{5.8} \) yr to a typical age for a classical radio galaxy of \( \sim 10^{7} \) yr suggests a source age ratio of \( \sim 7\% \). Combining this age ratio with the ratio in space density of \( \sim 0.3\% \) indicates that \( \sim 20\% \) of the classical radio galaxies might have been born directly from a WISE-NVSS source.

Finding alternate compact progenitors that might evolve into classical radio galaxies is not hard. O’Dea (1998) performs a similar demographic analysis with GPS and CSS sources and shows that they actually overproduce the classical radio galaxies by a factor of \( \sim 10 \). O’Dea (1998) interprets this apparent overproduction as evidence for recurrent activity in the GPS and CSS populations—meaning that there might be multiple phases of compact emission before the source finally evolves into a large-scale, classical, radio galaxy.

The relation between the WISE-NVSS sources and the GPS and CSS sources is not yet clear. There seems to be a systematic difference in the MIR properties (P. Patil et al. 2020, in preparation), suggesting that although all these sources may be dynamically young, the WISE-NVSS sources might be truly “newborn”—meaning that the radio source has emerged for the first time, into a dense near-nuclear ISM. In this case, the WISE-NVSS sources may either evolve directly into the classical radio galaxies or perhaps join the more common GPS and CSS classes, and from there ultimately evolve into a classical radio phase.

8. Summary and Conclusions

We have presented a high-resolution 10 GHz VLA imaging study of a sample of ultraluminous and heavily obscured quasars in the redshift range \( 0.4 < z < 3 \) with a median \( z \sim 1.53 \). Our selection is similar to that of Hot DOGs in MIR colors but adds a requirement for the presence of compact radio emission that allows us to select objects in which radio-emitting jets are present. Of the 155 radio sources in our sample, 86 \( (\sim 55\%) \) remain unresolved even on subarcsecond scales. Our main conclusions are as follows:

1. The compactness of the majority of the sources on scales \( < 0.2' \) implies that typical physical sizes are \( \lesssim 2 \) kpc at the median redshift \( (z = 1.53) \) of our sample.
2. We measured in-band spectral indices from 8–12 GHz and found a median spectral index of \( \sim 1.0 \), consistent with (perhaps slightly steeper than) typical optically thin synchrotron emission from radio jets or lobes.
3. We estimate equipartition pressures in the radio lobes and find them to be similar to other compact sources such as GPS or CSS sources, but significantly higher than the lobes of more extended classical radio galaxies. These high pressures support the possibility that the WISE-NVSS sources may be powered by recently triggered radio jets emerging into a dense, near-nuclear ISM.
4. Our radio sources have rest-frame 1.4 GHz luminosities between those of the classical FR I and FR II radio galaxies, in the range of \( 10^{25} \)–\( 10^{27.5} \) W Hz\(^{-1} \). On the well-known radio power versus linear size (PD) diagram, our sources fall in the same region as the other compact and medium-scale radio sources such as GPS and CSS sources.
5. We perform a standard V/V\(_{\text{max}}\) analysis to generate a 1.4 GHz radio luminosity function for our sample, and we compare it to other samples of radio sources. Overall, the WISE-NVSS sources are rare, with space densities roughly \( \sim 2–3 \) dex lower than the population of radio AGNs studied by Best et al. (2014) and \( \sim 0.5–1.0 \) dex lower than samples of compact radio AGNs (GPSs, HFPs; Snellen et al. 2000).
6. We use a simple adiabatic jet expansion model and an empirical relation between radio luminosity and jet power, to estimate dynamical ages, ambient densities, and expansion velocities for our sample sources. We find source ages in the range of \( 10^{4}–10^{5} \) yr (median 0.7 Myr), ambient particle densities in the range of \( 1–10^{4} \) cm\(^{-3} \) (median 101 cm\(^{-3} \)), and lobe expansion speeds in the range of 30–10,000 km s\(^{-1} \) (median 450 km s\(^{-1} \)). Within the framework of this model, these results broadly confirm our expectation that these sources are relatively young and are expanding at modest velocities into a relatively dense ISM, as suggested by their MIR–optical properties.
7. In the absence of unknown selection effects, such as variability (Mooley et al. 2016), our RLF and dynamical age analyses suggest that \( \sim 10\% \) of the population of large-scale radio galaxies could have evolved directly from the WISE-NVSS sources. The overabundance of the GPS and CSS sources relative to classical, large-scale radio sources raises the question of the relation between the WISE-NVSS sources and these other compact radio sources. We favor a scenario in which the WISE-NVSS sources harbor jets that have turned on for the very first time, following the merger and dumping of ISM into the nucleus. Following this initial phase, it is possible that the WISE-NVSS sources evolve into GPS or CSS sources, of which some ultimately evolve into the larger classical radio galaxies.

Overall, we conclude that the radio properties of our sample are consistent with emission arising from recently triggered, young jets. In a series of forthcoming studies, we will present an analysis of the broadband radio SEDs of our sources, as well as new milliarcsecond-scale-resolution imaging with the VLBA.
and enhanced Multi-Element Remotely Linked Interferometer Network (e-MERLIN). These studies will place tighter constraints on the source ages and provide deeper insights into their evolutionary stages. Ultimately, studies of the ISM content and conditions in the vicinity of young, ultraluminous quasars will be needed to investigate the onset and energetic importance of jet–ISM feedback during the peak epoch of galaxy assembly. Observations with ALMA and the James Webb Space Telescope, and eventually the next-generation VLA (e.g., Nyland et al. 2018; Patil et al. 2018), will be essential for improving our understanding of feedback driven by young radio AGNs at z ~ 2 and its broader connection to galaxy evolution.

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**Appendix A**

**Radio Lobe Expansion**

The mathematical treatment for the expansion of a spherical lobe driven by continuous energy input is given in Weaver et al. (1977). The momentum and energy conservation equations are

\[
\frac{d}{dt} \left( \frac{4}{3} \pi R_l^3 \rho_a V_l \right) = 4 \pi R_l^2 p_l, \tag{A1}
\]

\[
\frac{d}{dt} \left[ \frac{4 \pi}{3} \frac{p_l}{\gamma - 1} R_l^3 \right] + 4 \pi R_l^2 p_l V_l = F_E, \tag{A2}
\]

where \( R_l \) is the radius of the lobe’s shock, \( V_l = dR_l/dt \) is the velocity of the shock, \( \rho_a \) is the ambient density of the undisturbed ISM, \( p_l \) is the pressure inside the lobe, and \( F_E \) is the mechanical power injected by the jet. For a self-similar expansion of the jet lobe, the above equations can be solved to yield

\[
R_l = 0.78 F_{43}^{1/5} n_a^{-1/5} t_{\text{Myr}}^{3/5} \text{ kpc} \tag{A3}
\]

\[
p_l = 1.63 \times 10^{-9} F_{43}^{2/5} n_a^{-1/5} t_{\text{Myr}}^{-2/5} \text{ dynes cm}^{-2} \tag{A4}
\]

\[
V_l = 458 F_{43}^{1/5} n_a^{-1/5} t_{\text{Myr}}^{-2/5} \text{ km s}^{-1} \tag{A5}
\]

where \( F_{43} \) is in units of \( 10^{43} \text{ erg s}^{-1} \), \( n_a = \rho_a/(\mu m_p) \) is the ambient number density in \( \text{cm}^{-3} \), and \( t_{\text{Myr}} \) is a dynamical age in Myr. Here \( \mu m_p \) is the mean molecular weight of the ISM and \( m_p \) is the proton mass. Equations (A3)–(A5) can be rearranged to isolate \( t_{\text{Myr}}, n_a, \) and \( V_l \) in terms of our observed parameters:

\[
p_l = 7.76 \times 10^{-10} F_{43} t_{\text{Myr}}^{-3} R_l^{-3} \tag{A6}
\]

\[
p_l = 1.17 \times 10^{-9} F_{43}^{2/3} n_a^{1/3} R_l^{-4/3} \tag{A7}
\]

\[
p_l = 1.50 \times 10^{-12} F_{43} (V_l/c)^{-1} R_l^{-2}. \tag{A8}
\]
Appendix B
Observational Parameters

Observational details of our sample are provided in Table B1.

| Source | WISE ID | A-Array Obs Date (yyyy mm dd) | rms (μJy beam⁻¹) | S/N | Quality | B-Array Obs Date (yyyy mm dd) | rms (μJy beam⁻¹) | S/N | Quality |
|--------|---------|-------------------------------|------------------|-----|---------|-------------------------------|------------------|-----|---------|
| J0000+78 | 000035.88+780717.2 | 2012 Oct 31 | 19 | 383 | G | 2012 Jun 13 | 21 | 94 | G |
| J010+16 | 001039.54+164328.7 | 2012 Dec 1 | 20 | 87 | G | 2012 Jun 13 | 31 | 46 | G |
| J0104+27 | 010424.85+275029.0 | 2012 Nov 24 | 19 | 49 | G | 2012 Aug 27 | 27 | 175 | G |
| J0132+13 | 013211.24+130326.8 | 2012 Dec 1 | 22 | 202 | G | 2012 Aug 27 | 35 | 832 | G |
| J0133+10 | 013338.97+101943.9 | 2012 Dec 1 | 19 | 1064 | G | 2012 Aug 27 | 35 | 832 | G |

Note. Column (1): source name. Column (2): WISE ID. Column (3): date of observation for the A-array data. Column (4): 1σ rms noise level in the A-array continuum image. Column (5): source peak flux S/N. Column (6): a quality flag for the final continuum image. G = a good-quality image free of any artifacts or calibration issues; ND = no detection up to specified S/N; P = poor-quality image due to bad calibration or phase closure errors; F = pipeline failed to calibrate uv-data. We used images with G flags for our analysis. Columns (7)-(10): date of observation, 1σ rms noise, S/N of the source detection, and an image quality flag for the B-array observations.

(Appendix C
VLA Source Measurements

Beam sizes and source measurements from the VLA observations are given in Table C1. Results from JMFFT for source spatial measurements for the VLA A- and B-array observations are available in Table C2. Physical properties for our sample sources with redshift available are given in Table C3.

| Source | Array | Morph | θₘ × θₘ (″ × ″) | PA (deg) | Sₚ (mJy beam⁻¹) | Sₜot (mJy) | B-Array θₘ × θₘ (″ × ″) | PA (deg) | Sₚ (mJy beam⁻¹) | Sₜot (mJy) |
|--------|-------|-------|------------------|---------|-----------------|-------------|--------------------------|---------|-----------------|-------------|
| J0000+78 | A D | 0.3 × 0.1 | −13 | 13 | 7.1 ± 0.21 | 7.96 ± 0.22 | ... | ... | ... |
| J010+16 | A UR | 0.2 × 0.2 | 74 | 1.76 ± 0.06 | 1.87 ± 0.06 | 0.6 ± 0.06 | 17 | 1.97 ± 0.06 | 1.95 ± 0.07 |
| J0104+27 | A R | 0.5 × 0.1 | 14 | 0.68 ± 0.02 | 0.94 ± 0.15 | 2.0 ± 0.5 | −24 | 1.44 ± 0.05 | 1.42 ± 0.07 |
| J0132+13 | A SR | 0.2 × 0.2 | 20 | 4.32 ± 0.13 | 4.64 ± 0.14 | 0.6 ± 0.5 | −26 | 4.69 ± 0.14 | 4.70 ± 0.15 |
| J0133+10 | A D | 0.2 × 0.2 | 35 | 19.9 ± 0.6 | 34.6 ± 0.71 | 0.6 ± 0.5 | −25 | 28.28 ± 0.85 | 34.59 ± 0.85 |

Note. Column (1): source name. Column (2): the VLA array of the best continuum image. Column (3): source morphology based on the criteria defined in Section 4.3. UR = unresolved; SR = slightly resolved; R = fully resolved; D = double; T = triple; M = multicomponent sources. Column (4): synthesized beam of the A-array data (major axis, θₘ × minor axis, θₘ) in arcseconds. Column (5): position angle of the synthesized beam, measured counterclockwise from north. Column (6): peak flux density of the A-array image. Column (7): integrated flux of source A-array image. In case of multicomponent sources, we provide a sum total of fluxes from each component. Column (8): synthesized beam of the B-array data (major axis, θₘ × minor axis, θₘ) in arcseconds. Column (9): B-array beam position angle, measured counterclockwise from north. Column (10): peak flux density of the radio emission in the B-array image. Column (11): integrated flux in the B-array image.

(This table is available in its entirety in machine-readable form.)
| Source          | Region     | R.A.-A (hh:mm:ss.s) | Decl.-A (dd:mm:ss.s) | Source Size-A (mas × mas) | PA-A (deg) | R.A.-B (hh:mm:ss.s) | Decl.-B (dd:mm:ss.s) | Source Size-B (mas × mas) | PA-B (deg) | $\alpha_{\text{IB}}$ | S/N |
|----------------|------------|---------------------|----------------------|---------------------------|------------|---------------------|----------------------|--------------------------|------------|----------------|-----|
| J0000+78       | Reg 1      | 00:00:35.918        | 78:07:17.15          | <32                       | 158 ± 0    | ...                 | 00:10:39.531          | <126                     | 0 ± 5      | −1.71 ± 0.09 | 87  |
| Reg 2          | −15.72     | 5.82                | 163 ± 32 × 100 ± 10  | 54 ± 3                    | ...        | ...                 | ...                  | ...                      | ...        | −1.48 ± 0.38 | 27  |
| J0104−27       | Reg 1      | 01:04:24.862        | −27:50:29.16         | 976 ± 472                 | ...        | 01:04:24.867        | −27:50:28.98          | <262                     | 145 ± 0    | −1.71 ± 0.33 | 49  |
| J0132+13       | Reg 1      | 01:32:11.240        | 13:03:27.39          | 65 ± 4 × 23 ± 3           | 153 ± 2    | 01:32:11.239        | 13:03:27.39          | <127                     | 168 ± 2    | −1.26 ± 0.12 | 202 |
| J0133+10       | Reg 1      | 01:33:38.973        | 10:19:44.09          | <40                       | 105 ± 0    | 01:33:38.978        | 10:19:44.01          | 388 ± 2 × 60 ± 2       | 98 ± 0     | −1.01 ± 0.01 | 1065 |
| Reg 2          | 0.30       | −0.03               | 64 ± 1 × 56 ± 1      | 94 ± 1                    | ...        | ...                 | ...                  | ...                      | ...        | −1.46 ± 0.10 | 664 |

**Note.** Column (1): source name. Column (2): region. For a single-component source, the entire component is named Reg 1. For multicomponent sources, brightest radio emission component is named Reg 1. Columns (3) and (4): J2000 R.A. and decl. of the fitted source in the A-array image. In case of sources with more than one component, a source separation (in arcseconds) from the Reg 1 is provided. Column (5): deconvolved source sizes for the A-array data. If source is resolved only along the major axis, the deconvolved minor axis is specified as 0. In case of an unresolved source, we provide an upper limit on the major axis. A detailed description is provided in Section 4.2. For extended sources with non-Gaussian-like emission, we provide the size of 3$\sigma$ contour as the angular size of the respective region. Column (6): position angle of the fitted Gaussian, measured counterclockwise from north. Columns (7) and (8): J2000 R.A. and decl. for the B-array image. Column (9): B-array deconvolved source sizes from the JMFIT source fitting. Column (10): position angle for the fitted source. Column (11): in-band spectral index for the best image available. We used A-array data when a good-quality image is available. (see Section 4.4). Column (12): source detection S/N averaged from the 8.6 and 11.4 GHz images used for calculating $\alpha_{\text{IB}}$. (This table is available in its entirety in machine-readable form.)
### Table C3
Physical Properties for Our Sample Sources with Redshift Available

| Source  | $z$ | Region | Linear Size (kpc × kpc) | log$_{10}L_{1 + 60\mu m}$ (W Hz$^{-1}$) | $\alpha_{1.4}^{10}$ | log $P_l$ (dyne cm$^{-2}$) |
|---------|-----|--------|-------------------------|----------------------------------------|-------------------|---------------------------|
| J0010+16 | 2.85 | Reg 1 | <0.6 | 27.24 | $-1.20 \pm 0.03$ | $> -6.37$ |
| J0132+13 | 2.85 | Reg 1 | $0.5 \times 0.2$ | 27.07 | $-0.79 \pm 0.02$ | $-5.58$ |
| J0159+12 | 0.76 | Reg 1 | $1.7 \times 0.2$ | 25.78 | $-1.04 \pm 0.02$ | $-6.45$ |
| J0300+39 | 1.12 | Reg 1 | $0.7 \times 0.2$ | 25.92 | $-0.75 \pm 0.03$ | $-6.10$ |
| J0304+31 | 1.53 | Reg 1 | <0.2 | 26.73 | $-0.48 \pm 0.02$ | $> 5.08$ |
| J0306+33 | 0.78 | Reg 1 | <0.8 | 25.20 | $-0.77 \pm 0.05$ | $> 7.12$ |
| J0332+32 | 0.30 | Reg 1 | <0.1 | 25.13 | $-1.08 \pm 0.02$ | $> 5.69$ |
| J0342+37 | 0.47 | Reg 1 | <0.3 | 26.05 | $-0.48 \pm 0.02$ | $> 5.52$ |
| J0354+33 | 1.37 | Reg 1 | <0.8 | 25.78 | $-0.50 \pm 0.04$ | $> 6.74$ |
| J0404+24 | 1.26 | Reg 1 | $5.2 \times 3.8$ | 26.17 | $-1.38 \pm 0.09$ | $-8.55$ |
| J0409+18 | 0.67 | Reg 1 | <0.4 | 26.00 | $-1.08 \pm 0.02$ | $> 6.33$ |
| J0417+28 | 0.94 | Reg 1 | <0.4 | 25.69 | $-0.31 \pm 0.03$ | $> 6.05$ |
| J0439+31 | 2.82 | Reg 1 | $1.7 \times <0.0$ | 27.00 | $-0.71 \pm 0.02$ | $-6.99$ |
| J0519+08 | 2.05 | Reg 1 | <0.5 | 26.72 | $-0.55 \pm 0.02$ | $> 6.11$ |
| J0525+36 | 1.69 | Reg 1 | $1.3 \times 0.4$ | 25.77 | $-0.43 \pm 0.06$ | $-6.54$ |
| J0526+32 | 1.98 | Reg 1 | $4.4 \times 6.2$ | 27.64 | $-0.84 \pm 0.02$ | $> 5.90$ |
| J0536+27 | 1.79 | Reg 1 | <0.2 | 25.61 | $0.50 \pm 0.04$ | $> 4.41$ |
| J0549+37 | 1.71 | Reg 1 | <2.3 | 26.55 | $-1.48 \pm 0.04$ | $> 7.77$ |
| J0612+06 | 0.47 | Reg 1 | <0.5 | 25.48 | $-1.12 \pm 0.03$ | $> 6.87$ |
| J0613+34 | 2.18 | Reg 1 | <1.3 | 27.08 | $-1.24 \pm 0.03$ | $> 6.92$ |
| J0630+21 | 1.44 | Reg 1 | <0.3 | 25.97 | $-0.32 \pm 0.03$ | $> 6.33$ |
| J0642+27 | 1.34 | Reg 1 | $12.2 \times <0.0$ | 25.83 | $-0.93 \pm 0.07$ | $-9.33$ |
| J0652+20 | 0.60 | Reg 1 | <1.3 | 25.11 | $-1.20 \pm 0.04$ | $> 7.79$ |
| J0702+28 | 0.94 | Reg 1 | <0.5 | 25.32 | $-0.08 \pm 0.04$ | $> 6.36$ |
| J0714+36 | 0.88 | Reg 1 | <5.6 | 25.70 | $-1.05 \pm 0.03$ | $> 8.40$ |
| J0719+33 | 1.63 | Reg 1 | <0.2 | 26.40 | $-0.40 \pm 0.02$ | $> 5.25$ |
| J0729+65 | 2.24 | Reg 1 | <0.5 | 26.82 | $-0.91 \pm 0.02$ | $> 5.72$ |
| J0804+36 | 0.66 | Reg 1 | $0.4 \times 0.1$ | 26.24 | $-1.30 \pm 0.02$ | $-5.31$ |
| J0811+22 | 1.11 | Reg 1 | <3.1 | 26.17 | $-1.21 \pm 0.03$ | $> 7.90$ |
| J0823+06 | 1.75 | Reg 1 | <1.7 | 26.81 | $-0.39 \pm 0.06$ | $> 8.87$ |
| J0102+02 | 0.30 | Reg 1 | <1.9 | 24.42 | $-1.04 \pm 0.03$ | $> 8.23$ |
| J1107+34 | 1.45 | Reg 1 | $1.1 \times 0.2$ | 26.06 | $0.11 \pm 0.02$ | $-5.41$ |
| J1238+52 | 2.25 | Reg 1 | <0.6 | 27.53 | $-0.92 \pm 0.02$ | $> 5.92$ |
| J1308+34 | 1.65 | Reg 1 | $15.0 \times 4.3$ | 26.94 | $-0.59 \pm 0.02$ | $-7.86$ |
| J1343+11 | 2.49 | Reg 1 | <0.4 | 26.35 | $-0.49 \pm 0.04$ | $> 6.01$ |
| J1400+29 | 1.66 | Reg 1 | <0.5 | 27.17 | $-1.39 \pm 0.02$ | $> 6.19$ |
| J1412+20 | 1.81 | Reg 1 | $0.4 \times 0.1$ | 25.67 | $0.47 \pm 0.03$ | $-3.31$ |
| J1428+11 | 1.60 | Reg 1 | $4.7 \times 2.3$ | 26.34 | $-1.01 \pm 0.05$ | $-7.82$ |
| J1434+02 | 1.92 | Reg 1 | <0.6 | 27.04 | $-1.08 \pm 0.02$ | $> 6.30$ |
| J1439+37 | 1.20 | Reg 1 | <1.7 | 25.85 | $-0.74 \pm 0.04$ | $> 7.52$ |
| J1500+06 | 1.50 | Reg 1 | $1.4 \times 0.3$ | 26.60 | $-1.30 \pm 0.03$ | $-6.56$ |
| J1501+13 | 0.51 | Reg 1 | <0.4 | 26.52 | $-1.58 \pm 0.02$ | $> 6.05$ |
| J1510+22 | 0.95 | Reg 1 | <0.5 | 25.85 | $-0.74 \pm 0.03$ | $> 6.23$ |
| J1513+22 | 2.20 | Reg 1 | $1.3 \times 1.6$ | 27.07 | $-1.01 \pm 0.02$ | $-6.99$ |
| J1514+34 | 1.08 | Reg 1 | <0.9 | 25.81 | $-0.66 \pm 0.03$ | $> 6.89$ |
| J1517+35 | 1.51 | Reg 1 | <1.1 | 26.92 | $-1.30 \pm 0.02$ | $> 6.92$ |
| J1521+00 | 2.63 | Reg 1 | <0.1 | 26.75 | $0.08 \pm 0.02$ | $> 4.13$ |
| Source   | $z$   | Region | Linear Size (kpc × kpc) | log$_{10} L_{1.4 \text{ GHz}}$ (W Hz$^{-1}$) | $\alpha_{1.4}^{10}$ | log $P_e$ (dyne cm$^{-2}$) |
|----------|-------|--------|------------------------|-----------------------------------------------|----------------------|--------------------------|
| J1541−11 | 1.58  | Reg 1  | <0.9                   | 27.22                                          | −2.09 ± 0.03         | > −7.08                   |
| J1630+51 | 0.72  | Reg 1  | <0.6                   | 26.30                                          | −0.49 ± 0.02         | > −6.17                   |
| J1634−17 | 2.07  | Reg 1  | <0.8                   | 26.77                                          | −1.55 ± 0.06         | > −7.14                   |
| J1641−05 | 1.83  | Reg 1  | <1.0                   | 26.30                                          | −1.20 ± 0.04         | > −7.18                   |
| J1642−41 | 1.28  | Reg 1  | <0.9                   | 26.32                                          | −0.89 ± 0.02         | > −6.74                   |
| J1653−01 | 2.02  | Reg 1  | <0.6                   | 26.28                                          | −0.38 ± 0.03         | > −6.18                   |
| J1702−08 | 2.85  | Reg 1  | 1.1 × 0.3              | 27.57                                          | −0.81 ± 0.02         | > −5.67                   |
| J1703+26 | 1.07  | Reg 1  | <0.2                   | 26.42                                          | −0.52 ± 0.02         | > −5.07                   |
| J1703−05 | 1.79  | Reg 1  | 0.3 × 0.2              | 26.47                                          | −0.22 ± 0.02         | > −5.71                   |
| Reg 2    |       |        | 1.3 × 0.6              | ...                                            | ...                  | −6.26                     |
| J1717+53 | 2.72  | Reg 1  | <0.3                   | 26.74                                          | −0.35 ± 0.02         | > −5.55                   |
| J1936−33 | 2.24  | Reg 1  | <3.3                   | 26.44                                          | −1.22 ± 0.06         | > −8.07                   |
| J1951−04 | 1.58  | Reg 1  | <0.4                   | 26.73                                          | −1.46 ± 0.04         | > −6.07                   |
| Reg 2    |       |        | 9.3 × 1.5              | ...                                            | ...                  | −8.14                     |
| J1958−07 | 1.80  | Reg 1  | <0.9                   | 26.91                                          | −1.06 ± 0.02         | > −6.46                   |
| J2000−28 | 2.28  | Reg 1  | <0.8                   | 26.66                                          | −0.72 ± 0.03         | > −6.13                   |
| J2021−26 | 2.44  | Reg 1  | 2.8 × 0.5              | 26.58                                          | −1.09 ± 0.05         | −6.93                     |
| J2059−35 | 2.38  | Reg 1  | 20.2 × 10.1            | 27.11                                          | −1.92 ± 0.23         | −9.30                     |
| J2126−01 | 0.61  | Reg 1  | <0.3                   | 25.34                                          | −1.09 ± 0.04         | > −6.50                   |
| J2130+20 | 0.81  | Reg 1  | <2.8                   | 26.44                                          | −1.06 ± 0.04         | > −8.27                   |
| Reg 2    |       |        | 32.7 × 29.3            | ...                                            | ...                  | −9.68                     |
| J2226+00 | 0.68  | Reg 1  | 4.4 × 3.9              | 25.59                                          | −1.17 ± 0.06         | −8.19                     |
| J2330−07 | 0.44  | Reg 1  | 1.3 × 0.5              | 25.56                                          | −1.07 ± 0.02         | −6.76                     |
| J2318+25 | 0.50  | Reg 1  | 147.4 × 70.3           | 26.15                                          | −1.02 ± 0.12         | −9.34                     |
| Reg 2    |       |        | 56.2 × 31.2            | ...                                            | ...                  | −9.20                     |
| J2325−04 | 1.74  | Reg 1  | 2.9 × 1.2              | 27.46                                          | −0.90 ± 0.02         | −6.62                     |
| Reg 2    |       |        | 2.9 × 1.2              | ...                                            | ...                  | −6.65                     |
| J2332+34 | 0.98  | Reg 1  | <0.5                   | 25.96                                          | −1.31 ± 0.03         | > −6.73                   |
| J2357−10 | 2.05  | Reg 1  | <0.4                   | 26.57                                          | −0.80 ± 0.03         | > −6.05                   |

Note. Column (1): source name. Column (2): redshift. Column (3): region name. Column (4): linear dimensions of the radio emission in each region. For an unresolved source, we use an upper limit on the angular major axis to estimate the limit on the source linear size. Column (5): rest-frame 1.4 GHz luminosity. We use NVSS flux and the spectral index between NVSS and 10 GHz continuum observations to calculate the luminosity. Column (6): spectral index between NVSS and 10 GHz observations. Fluxes from all of the regions are added up to estimate the spectral indices. Column (7): equipartition lobe pressures as described in Section 5.4.

(This table is available in machine-readable form.)
Appendix D
10 GHz Continuum Images

We provide individual 10 GHz continuum images of our sample in the online Figure Set associated with Figure D1.

The complete figure set (162 images) is available.
Appendix E
Sources with Extended Emission

We classified radio morphologies by visually inspecting our VLA images, as well as several archival radio surveys, namely, TGSS, NVSS, FIRST, and VLASS (see Sections 4.3 and 5.1 for details). We find that 25/155 sources have well-extended, complex radio emission on a few arcsecond scales either in our 10 GHz data or in other radio surveys. Table E1 provides morphological classes and angular extents for those 25 sources in each of the surveys mentioned above except the NVSS. Figure E1 compares image cutouts taken from these five radio surveys.

Table E1
List of Extended Sources

| Source   | VLA-X Morphology | VLASS Morphology | FIRST Morphology | TGSS Morphology | Angular Extent VLA-X (arcsec) | Angular Extent VLASS (arcsec) | Angular Extent FIRST (arcsec) | Angular Extent TGSS (arcsec) |
|----------|------------------|------------------|------------------|-----------------|-------------------------------|-------------------------------|-------------------------------|-------------------------------|
| J0000+78 | UR               | T                | ...              | R               | 0.04                          | 22.1                          | ...                           | 33.4                          |
| J0010+16 | UR               | UR               | ...              | T               | 0.07                          | 2.5                           | ...                           | 153.1                         |
| J0132+13 | SR               | UR               | ...              | D               | 0.07                          | 2.4                           | ...                           | 47.4                          |
| J0342+37 | UR               | UR               | ...              | D               | 0.04                          | 2.9                           | ...                           | 44.3                          |
| J0543+52 | T                | D                | ...              | UR              | 5.3                           | 4.5                           | ...                           | 12.0                          |
| J0602+27 | T                | D                | ...              | R               | 4.4                           | 4.3                           | ...                           | 26.6                          |
| J0737+18 | D                | D                | UR               | R               | 9.3                           | 8.9                           | 5.4                           | 29.4                          |
| J1025+61 | T                | T                | D                | D               | 46.1                          | 46.8                          | 47.3                          | 47.6                          |
| J1138+20 | UR               | D                | D                | ...             | 0.02                          | 13.8                          | 14.3                          | ...                           |
| J1308−34 | T                | T                | ...              | R               | 8.9                           | 9.7                           | ...                           | 37.1                          |
| J1439−37 | D                | D                | ...              | R               | 11.2                          | 15.3                          | ...                           | 48.5                          |
| J1525+76 | UR               | T                | ...              | D               | 0.11                          | 46.6                          | ...                           | 40.4                          |
| J1651+34 | M                | D                | D                | R               | 12.6                          | 12.8                          | 11.9                          | 15.0                          |
| J1703−05 | D                | D                | ...              | R               | 6.2                           | 7.0                           | ...                           | 13.2                          |
| J1951−04 | T                | T                | ...              | D               | 24.3                          | 29.5                          | ...                           | 39.9                          |
| J2059−35 | SR               | R                | ...              | D/R             | 2.4                           | 5.3                           | ...                           | 51.3                          |
| J2124−28 | M                | T                | ...              | R               | 11.4                          | 11.2                          | ...                           | 30.5                          |
| J2130−20 | T                | T                | ...              | D               | 39.1                          | 37.1                          | ...                           | 44.8                          |
| J2133−17 | T                | T                | ...              | R               | 18.8                          | 20.5                          | ...                           | 25.2                          |
| J2145−06 | D                | D                | D                | UR              | 3.4                           | 10.4                          | 10.2                          | 25.0                          |
| J2212−12 | T                | T                | ...              | R               | 20.9                          | 20.0                          | ...                           | 26.8                          |
| J2318+25 | T                | T                | ...              | R               | 34.7                          | 36.9                          | ...                           | 70.4                          |
| J2328−02 | SR               | D                | D                | UR              | 0.13                          | 14.6                          | 12.1                          | 25.0                          |
| J2331−14 | D                | D                | ...              | R               | 7.2                           | 8.3                           | ...                           | 17.6                          |
| J2341−29 | UR               | D                | ...              | R               | 0.11                          | 5.7                           | ...                           | 40.6                          |

Note. Column (1): source name. Columns (2)–(6): source morphologies in our 10 GHz VLA data, VLASS, FIRST, and TGSS, respectively. The morphological classes are as follows: UR = unresolved; SR = slightly or marginally resolved; D = double; T = triple; M = multicomponent sources. The detailed description of morphological classes is given in Section 4.3. Columns (6)–(9): largest angular extent in arcseconds for the radio emission detected in our 10 GHz VLA survey, VLASS, FIRST, and TGSS, respectively. For sources with a single-component emission, we provide angular size estimates from their respective source catalogs. For multicomponent sources, we provide largest source separation measured manually using the CASA Viewer. (This table is available in machine-readable form.)
Figure E1. Radio continuum cutouts of our sample sources that have extended emission on angular scales greater than a few arcseconds. The source name is shown to the left of the first column, and the name of the radio survey is shown above the first row of cutouts. The red circle corresponds to the typical angular resolution of NVSS (=45″). The synthesized beam is shown as a purple ellipse in the lower-left corner. A white solid line on the lower-right denotes the scale bar. The tick mark spacing is equal to the length of the scale bar.

(The complete figure set (25 images) is available.)
Weaver, R., McCray, R., Castor, J., Shapiro, P., & Moore, R. 1977, ApJ, 218, 377
Weston, M. E., McIntosh, D. H., Brodwin, M., et al. 2017, MNRAS, 464, 3882
Willott, C. J., Rawlings, S., Blundell, K. M., & Lacy, M. 1999, MNRAS, 309, 1017
Worrall, D. M., & Birkinshaw, M. 2000, ApJ, 530, 719
Wright, E. L., Eisenhardt, P. R. M., Mainzer, A. K., et al. 2010, AJ, 140, 1868
Wu, J., Tsai, C.-W., Sayers, J., et al. 2012a, ApJ, 756, 96
Wu, X.-B., Hao, G., Jia, Z., Zhang, Y., & Pong, N. 2012b, AJ, 144, 49
York, D. G., Adelman, J., Anderson, J. E., Jr., et al. 2000, AJ, 120, 1579