Improving dynamical mass constraints for intermediate-period substellar companions using Gaia DR2

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ABSTRACT

The relationship between luminosity and mass is of fundamental importance for direct imaging studies of brown dwarf and planetary companions to stars. In principle this can be inferred from theoretical mass-luminosity models; however, these relations have not yet been thoroughly calibrated, since there is a lack of substellar companions for which both the brightness and mass have been directly measured. One notable exception is GJ 758 B, a brown dwarf companion in a ~20 AU orbit around a nearby Sun-like star, which has been both directly imaged and dynamically detected through a radial velocity trend in the primary. This has enabled a mass constraint for GJ 758 B of $42^{+4}_{-5}$ $M_{\text{Jup}}$. Here, we note that Gaia is ideally suited for further constraining the mass of intermediate-separation companions such as GJ 758 B. A study of the differential proper motion, $\Delta \mu$, with regards to HIPPARCOS is particularly useful in this context, as it provides a long time baseline for orbital curvature to occur. By exploiting already determined orbital parameters, we show that the dynamical mass can be further constrained to $42.4^{+0.4}_{-0.5} M_{\text{Jup}}$ through the Gaia-HIPPARCOS $\Delta \mu$ motion. We compare the new dynamical mass estimate with substellar evolutionary models and confirm previous indications that there is significant tension between the isochronal ages of the star and companion, with a preferred stellar age of $\geq 5$ Gyr while the companion is only consistent with very old ages of $\geq 8$ Gyr.

Key words. astrometry — brown dwarfs — stars: kinematics and dynamics

1. Introduction

Multiple systems of stars and substellar companions prove to be excellent benchmarks to be compared with evolutionary models, as their dynamical motions can yield model-independent masses provided that their orbits can be constrained. The systems become even more valuable if their ages can be accurately determined, as they provide a means to calibrate the evolutionary models directly from what is observed. For low-mass multiple systems, evolutionary models generally underpredict the mass by a factor of 10 – 30% compared to the dynamical estimates (e.g. [Montet et al. 2015] Calissendorff et al. 2017). In the even-lower-mass regimes, towards substellar brown dwarfs, detected multiple systems with constrained orbits become less frequent, leading to a higher degree of uncertainty in the predictions by the models (e.g. [Dupuy et al. 2009]).

Astrometric monitoring of substellar companions on long orbits typically requires a good portion of the orbit to be covered in order to yield any robust results. Nevertheless, in some cases, the companion imposes a strong gravitational pull on its host, sufficient for producing a measurable Doppler shift, which can aid in the determination of the orbit and mass of the system. Although the companion may not always be resolvable, precise astrometric measurements like those of HIPPARCOS (Perryman et al. 1997) and Gaia (Gaia Collaboration et al. 2016) may reveal insights to the small astrometric perturbation the companions have on their host star. Given the timescale between two proper motion measurements, and the acceleration of the companion, a shift in proper motion for the entire system can potentially be detected and used to infer more stringent dynamical mass solutions for suitable targets.

GJ 758 is a bright solar-type $\approx$ G8 star with $V = 6.3$ mag, located at a distance of $d = 15.76 \pm 0.9$ pc (van Leeuwen 2007), and slightly enhanced metallicity of [Fe/H] = 0.18 \pm 0.05 (Vigan et al. 2016). While the age of the system has long been uncertain, with estimations ranging from $\approx 40$ Myr to $\approx 10$ Gyr, most estimations point towards older ages of several Gyrs (e.g. Janson et al. 2011). Combining HIPPARCOS parallax and proper motions by van Leeuwen (2007) with absolute radial velocity by Nidever et al. (2002) yields space velocities of $(U, V, W) = (-21.1 \pm 0.2, -14.1 \pm 0.5, -3.0 \pm 0.2)$ km/\text{s}, which places the system close to the $\sim 40$ Myr-old Argus association (BANYAN II tool, Gagné et al. 2014). When taking into account information from both photometry and kinematics, the updated BANYAN $\Sigma$-tool instead estimates with a 99.4% probability that GJ 758 is an old field star (Gagné et al. 2018). However, it should be pointed out that the Argus association is not included in the BANYAN $\Sigma$ analysis, as the association itself may be contaminated and not be considered as coeval (Bell et al. 2015). Chemical tagging of the star further supports an older age for the system and rules out Argus association membership. For young stars, lithium can be used as a sensitive age indicator, typically traced by the Li 6708 Å resonance line. The lack of lithium observed by Vigan et al. (2016) sets a stringent lower limit of the age of $\sim 600$ Myr; at this age, detectable amounts of lithium should have vanished for stars with the colours exhibited by GJ 758. Future asteroseismology studies may help to refine the age estimate further.

The companion, GJ 758 B, was first detected with the Subaru/HICIAO by Thalmann et al. (2009), and is likely to be a late T-type brown dwarf companion. Depending on the adopted age of the system, evolutionary models predict masses for the com-
panion of between 10 and 40 $M_{\odot}$ (Janson et al. 2011; Nilsson et al. 2017; Bowler et al. 2018). However, evolutionary models are highly uncertain at these low masses. The companion is close enough to its host star that its gravitational influence is measurable with radial velocity (RV), yet well enough separated that both components can be resolved and characterised with direct imaging. The imaging combined with the long-term RV trends observed make the companion an especially useful benchmark object, as only a handful of similar systems have been detected so far.

By combining high-contrast imaging astrometric data of GJ 758B and the observed radial velocity trends, Bowler et al. (2018) employ a Monte Carlo Markov Chain (MCMC) simulation in order to estimate a dynamical mass for the companion of $42^{+10}_{-19} M_{\odot}$, independent of the age of the system. Assuming that both GJ 758 and its companion are coeval, isochrones from evolutionary models then predict from the mass of the companion that the system is likely to be older than a few gigayears.

Using the marginalised posteriors of the fitted orbital parameters from the MCMC analysis made by Bowler et al. (2018), we construct our own simulation in order to predict which orbits are compatible with the proper motion of the system measured by Gaia in DR2 (Gaia Collaboration et al. 2018b). We adopt the distance parallax $\pi_{\text{HIPPARCOS}} = 63.45 \pm 0.35$ mas from van Leeuwen (2007) in order to be consistent with the simulations by Bowler et al. (2018). For the proper motions of GJ 758, we adopt the HIPPARCOS values from Perryman et al. (1997) of $\mu_{\text{HIPPARCOS}} = 82.04 \pm 0.54$ mas yr$^{-1}$ and $\mu_{\text{HIPPARCOS}} = 162.92 \pm 0.52$ mas yr$^{-1}$, which are compared to the Gaia proper motions, $\mu_{\text{Gaia}} = 81.80 \pm 0.03$ mas yr$^{-1}$ and $\mu_{\text{Gaia}} = 160.39 \pm 0.04$ mas yr$^{-1}$.

First, we extract the posterior distributions from the histograms in Bowler et al. (2018) using the online webtool WebPlotDigitizer (Rohatgi 2018). For each parameter, we then calculate the cumulative density function (CDF) and take $N = 20,000$ uniformly distributed random points between 0 and 1 that we translate using the CDFs into trial points for each parameter. We calculate the orbit for each set of orbital parameters simulated in this way and calculate the positional angle (PA) and relative separation at the epochs of the astrometric data points.

We then compare the predicted values to the relative astrometry of Bowler et al. (2018) with a $\chi^2$-test weighted by the errors in the astrometry and save the $n_t = 100$ best orbits. This procedure is required in order to remove infeasible combinations of orbital parameters related to covariances in the data. The procedure is repeated $n_t = 200$ times until we have 20,000 saved orbits.

From the saved orbits, we can predict the position of the companion during the HIPPARCOS and Gaia epochs. Using the HIPPARCOS Intermediate Astrometric Data tool (2018), we identify the orbits (and thereby epochs) during which GJ 758 was observed. This gives us 21 unique orbits in which the target was observed. We then estimate the position of the companion for each observed epoch and calculate the proper motion value for the companion as the difference in position divided by the time between the observations. We thereafter take the median value for the proper motion of the companion at the HIPPARCOS epoch of 1991.25 as $\mu_{\text{HIPPARCOS}}$. Using instead the first and last observed epochs divided by the time difference yields similar proper motions for the simulated orbits, with a median discrepancy of $\leq 20$ mas. For the Gaia epochs, we use the Gaia Observation Forecast Tool (2017) to estimate the orbits and dates during which GJ 758 was observed. We find 18 unique predicted epochs within the time-frame of 25 July 2014 (10:30 UTC) and 23 May 2016 (11:35 UTC) on which the Gaia DR2 data is based, and note that this is more than the 16 epochs that were used for calculating the astrometric solution during the visible periods.

Without knowing which exact epochs were used in the astrometry, we include all of them in our calculations and employ the same methods as before to estimate the companion proper motion at the Gaia epoch at 2015.50 as $\mu_{\text{Gaia}}$. We then calculate the difference in proper motion between the two epochs for the companion as

$$\Delta \mu_{c} = \mu_{\text{Gaia}} - \mu_{\text{HIPPARCOS}}.$$  

and scale the difference in proper motion for the companion up to the star as

$$\Delta \mu_{*} = \frac{\Delta \mu_{c}}{\mu_{*}} + 1,$$

where the $+1$ is added to the denominator to account for the fact that in the companion imaging we measure the companion position relative to the photocentre instead of relative to the centre of mass. The contrast in brightness between the primary and the companion causes the astrometric position of the system to be unaffected by the presence of the companion. As the companion is expected to be very dark in the Gaia band, the photocentre is centred on the primary.

This provides us with a set of 20,000 predicted values for the difference in proper motion between the two epochs, as shown in Fig. 1. The median values for the predicted difference in proper motions are $\Delta \mu_{\text{RA}} = -0.61$ mas yr$^{-1}$ and $\Delta \mu_{\text{DEC}} = -2.80$ mas yr$^{-1}$, respectively. We then compare these predicted values with the actual difference using the new Gaia DR2 value. The predicted $\Delta \mu_{c}$ values that coincide within the uncertainty of measured values of $\Delta \mu_{\text{RA}} = -0.24 \pm 0.54$ mas yr$^{-1}$ and $\Delta \mu_{\text{DEC}} = -2.53 \pm 0.52$ mas yr$^{-1}$ provide us with a family of simulated trial points that correspond to allowed orbits, which are plotted in Fig. 2. Approximately one third of the 20,000 simulated trial values were accepted.

For the allowed orbits, we obtain the respective companion masses, seen in the histogram in Fig. 3. For the most probable value, we find the most commonly populated mass bin and take the median value inside the bin, yielding a companion mass of $M_c = 42.4_{-5.0}^{+5.5} M_{\odot}$, where the error is taken as the limits of the minimum range that enclose 68.27% of the allowed values. The 20,000 saved orbits in the simulation that were best fitted to the relative astrometry are also shown in Fig. 3 for which we obtain a companion mass of $40^{+19}_{-15} M_{\odot}$, reproducing a similar distribution to the original simulation by Bowler et al. (2018). We note that there are differences between the HIPPARCOS proper motions as calculated in Perryman et al. (1997) and van Leeuwen (2007), respectively, which exceed their formal error bars. This reflects the difference between the two measured $\Delta \mu$ values plotted in Fig. 1 where the measured differences in proper motions for the van Leeuwen (2007) solution are measured as $\Delta \mu_{\text{RA}} = -1.60 \pm 0.34$ mas yr$^{-1}$ and $\Delta \mu_{\text{DEC}} = -1.93 \pm 0.30$ mas yr$^{-1}$. Therefore, while the Perryman et al. (1997) astrometry results are observed for the Gaia epoch at 2015.50 as $\mu_{\text{Gaia}}$. We then calculate the difference in proper motion between the two epochs for the companion as

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overlaps with our simulated values as expected, the van Leeuwen (2007) reduction deviates beyond the error bars in right ascension space. However, in declination space, the two reductions are consistent within error bars, and this is the direction along which most of our expected acceleration takes place over the relevant baseline. The difference between the reductions therefore does not have a significant impact on the mass estimation. Replacing the proper motion value in declination for the van Leeuwen (2007) solution yields a companion mass of $39M_{\text{Jup}}$, which is within the error bars of the formally stated result.

We further probe the impact of the updated parallax value from Gaia DR2 of $\pi_{\text{Gaia}} = 64.06 \pm 0.02$ mas and the original parallax solution for HIPPARCOS by Perryman et al. (1997) of $\pi_{\text{perryman}} = 64.54 \pm 0.60$ mas. The change in distance has little impact on the constraints on the dynamical mass, and we subsequently obtain companion masses of $M_c,\pi_{\text{Gaia}} = 42.4^{+5.1}_{-5.8} M_{\text{Jup}}$ and $M_c,\pi_{\text{perryman}} = 42.5^{+4.2}_{-3.5} M_{\text{Jup}}$. We verify from the original catalogues that both of the HIPPARCOS and Gaia astrometry are calculated using a five-parameter solution, and that the system has been treated as a single star for the reduction (Perryman et al. 1997; van Leeuwen 2007; Lindegren et al. 2016). We confirm from the HIPPARCOS Intermediate Data Tool that there were no outliers or other signs of bias to the proper motion in the data. We also check that the correlation between proper motions in right ascension and declination, $\rho(\mu_{\alpha}, \mu_\delta)$, is consistent between the two catalogues, estimated as $-0.05$ and $-0.03$ for the HIPPARCOS and the Gaia catalogues, respectively.

Using the previously calculated orbits for a binary system with long RV trends, we can compare the difference in proper motion, $\Delta \mu$, between the HIPPARCOS and Gaia epochs in order to further constrain the previous dynamical mass estimates. Here, we employ our method by re-simulating posterior distributions from orbital fits and determine which orbits are consistent with the measured difference in proper motions. Wielen et al. (1999) use a similar approach to identify binaries from long-term ground-based proper motions and HIPPARCOS, arguing that a statistically significant difference in proper motion with respect to the measurement errors could be due to the prevalence of unseen companions. In Wielen et al. (1999), the proper motion component caused by orbital motion of an intermediate-period companion is assumed to largely cancel out over the very long baseline of the ground-based data, while the HIPPARCOS astrometry retains an orbital motion term in its (approximately instantaneous) proper-motion measurement. The differential proper motion therefore contains a companion signature, although there is considerable ambiguity in the properties of the implied companion. The same procedure could in principle be applied to the Gaia data relative to ground-based data. However, in the case of GI 758, we already have prior information on the orbit, so in this case it is better to relate the Gaia astrometry to the HIPPARCOS astrometry, to get a more precise constraint on the mass without the ambiguities of the original Wielen et al. (1999) approach.

The exploitation of difference in proper motion between HIPPARCOS and Gaia DR1 was also discussed by Lindegren et al. (2016). They define the statistic $\Delta Q$ as a measure of the difference in proper motion between the Tycho-Gaia Astrometric Solution (TGAS) subset of DR1 and the HIPPARCOS catalogue, normalised by the covariances. They divide the sample into two groups; the first one including $\approx 90,000$ bona fide single...
stars with an astrometric five-parameter solution, and the second sample with \( N = 9000 \) stars that include solutions accounting for binaries and acceleration. Surprisingly, the distribution in relative frequency over \( \Delta Q \) is similar for the two groups, and differs from the expected theoretical distribution. Lindegren et al. (2016) argue that this effect could be an underestimation of the uncertainties in the catalogues, and the fact that most stars are non-single causes the cosmic scatter to be a real effect. Nevertheless, the non-single star sample displays a higher \( \Delta Q \) relative frequency, which confirms the sensitivity of the statistic as a probe for duplicity and unseen companions. Indeed, GJ 758 is in the single star sample, displaying a \( \Delta Q = 20 \), which is on the higher end of the distribution. This is comparable to similar systems with substellar companions that are treated as single stars such as HD 4747, which has a \( \Delta Q \)-value above 130, and HR 7672 with a value above 300. Therefore, bona fide single stars in the sample with high \( \Delta Q \) values require special attention and may be revealed to host substellar companions.

3.2. Astrometric solution & primary component

We note that brightness of GJ 758 with \( G = 6.1 \) mag is close to the optimal limit for Gaia (see e.g. Lindegren et al. 2018). For brighter stars, the parameters obtained for the DR2 require careful interpretations. The astrometric excess noise in the DR2 characterises the nature of the solution as a good fit for the source, and is only equals to zero if all observations fit the single-star model well enough. For GJ 758, the quantity is estimated as 0 mas, the same as for other, similar systems such as HD 4747 and HD 4113 that are slightly fainter and thus coincide with the optimal brightness range for Gaia. In comparison, the slightly brighter system GJ 504 with a magnitude of \( G = 5.0 \) mag displays an astrometric excessive noise of 0.59 mas. When we apply our proper-motion test to GJ 504 and its companion we are unable to produce trial \( \Delta \mu \)-values that coincide with the measured values. Although the curvature of the orbit of the companion in the case of GJ 504 is small and the predicted proper motion values are difficult to measure, we cannot exclude the possibility that discrepancy in predicted and measured \( \Delta \mu \) stems from the excessive noise in the data for GJ 504 due to its bright nature. Furthermore, a \( \chi^2 \) fit to the residuals of the along-scan measurements performed by Gaia is used as an alternative measure for how well the single-star model fits the source. For GJ 758, the quantity is measured to \( \chi^2_{\text{Gaia}, \ GJ 758} \approx 530 \), comparable to HD 4747 with \( \chi^2_{\text{HD}, \ 4747} \approx 280 \) and significantly lower than the brighter GJ 504 system with \( \chi^2_{\text{Gaia}, \ GJ 504} \approx 4600 \).

Beyond the solar system, all sources are treated as point objects and single stars in the Gaia DR2, and their motions are described by a five-parameter model (Lindegren et al. 2018). Therefore, it is the photocentre that is used for the astrometric solution and not the centre of mass. We scrutinise the Gaia source catalogue and find no available photometric variability flags that may bias the astrometric solution. Nevertheless, the orbital motion may affect the astrometric solution, albeit the effect is expected to be small given the low mass ratio of \( q = 0.04 \) and the relative motion of the companion during the Gaia observations.

We assumed a primary stellar mass of \( 0.97 \pm 0.02 \, M_\odot \), which is the best fit to the simulations by Bowler et al. (2015). The value for the stellar mass stems from Vigan et al. (2016), where evolutionary models by Bressan et al. (2012) were employed with an assumed age of \( 2.2 \pm 1.4 \) Gyr. However, the dynamical mass for the companion implies an older age of \( \gtrsim 8 \) Gyr, which in turn would be more consistent with a smaller stellar mass according to the models, bringing the components closer to each other in the mass-luminosity diagram. We therefore probe the effect of having a lower stellar mass of \( M_\star \approx 0.91 \, M_\odot \), to be more consistent with an older age for the primary, and increase the uncertainty to \( \pm 0.1 \, M_\odot \). We note that this has little impact on our results, with a slightly lower companion mass of \( 41.5^{+5.5}_{-4.5} \, M_{\text{Jup}} \), which is well within the error bars of the formally stated companion mass.

3.3. Conclusions and outlook

We obtain a new, more precise dynamical mass-estimate for GJ 758B of \( 42.4^{+5.6}_{-5.4} \, M_{\text{Jup}} \), which can be used to test substellar evolutionary models. We compare GJ 758B in a mass-luminosity diagram using isochrones ranging ages 1 - 10 Gyr from the COND evolutionary models (Baraffe et al. 2003) and the bolometric luminosity of \( \log(L/L_\odot) = -6.07 \pm 0.03 \) (Bowler et al. 2018), shown in Fig. 6. The models predict an age of \( \approx 8 \) Gyr for the companion, which is older than previous estimates for the primary host. This age discrepancy and uncertainty is similar to that of the GJ 504 system, for example, which also hosts a companion with a long-standing ambiguity in its mass (e.g. D’Orazi et al. 2017), further illustrating the difficulty of determining ages of intermediate-age Sun-like stars, and the importance of dynamical mass measurements for their companions. GJ 758B thereby joins a growing list of cool, T-type substellar companions on medium long periods of \( \approx 30-100 \) years, imaged around solar-type main sequence stars such as GJ 504b, HD 4113C, and HD 4747B (Kuzuhara et al. 2013; Cheetham et al. 2017; Crepp et al. 2018).

Due to the favourable orbit and the observational data available for GJ 758B, the method we employ works well. For the similar systems described above, only HD 4747B has such an orbit for which \( \Delta \mu \) can be properly estimated. However, the period of HD 4747B is \( \approx 38 \) years, and already has a well-constrained mass of \( 65.3^{+13.4}_{-3.4} \, M_{\text{Jup}} \). This means that we can apply a sanity check to our methodology by applying the same method as described above to HD 4747B, in order to check if the precise \( \Delta \mu \) prediction allowed by the existing orbital fit matches the Gaia DR2 data. We confirm that this is indeed the case, with a measured \( \Delta \mu \) of \( 1.63 \pm 1.10 \) mas yr\(^{-1}\) in right ascension and \( 4.33 \pm 0.81 \) mas yr\(^{-1}\) in declination for HD 4747. The predicted \( \Delta \mu \) values for HD 4747 range from 1 to 6 mas yr\(^{-1}\) with a median of 2.7 mas yr\(^{-1}\) in right ascension and from 2 to 6 mas yr\(^{-1}\) with a median of 3.38 mas yr\(^{-1}\) in declination. The trial orbits consistent with the measured \( \Delta \mu \) values yield a mass of \( M_{\text{HD}, \ 4747B} = 64.1^{+12.6}_{-4.6} \, M_{\text{Jup}} \). For the case of HD 4747, the astrometry is consistent between the two reductions, and both are consistent with our simulated predictions. We suggest that future studies involving the \( \Delta \mu \) between HIPPARCOS and Gaia should consider both existing HIPPARCOS reductions, note whether there are systematic differences between them, and if so, compare the resulting \( \Delta \mu \) values to see if the specific reduction has an effect on the result.

A reasonable assumption is that both components in the GJ 758 system are coeval, and that the age of the companion can be used to place constraints on the host and thereby entire the system. However, at these very low substellar masses, evolutionary models are not well-constrained and generally underpredict masses based solely on the brightness of an object. Therefore, precise dynamical mass-estimates of substellar objects such as GJ 758B can be used as touchstone objects for calibrating evolutionary models at substellar masses. The fact that GJ 758B is likely to be one of the lowest-mass and coldest substellar
The observations demonstrate the power of \textit{Gaia} for constraining the properties of wide companions, particularly with the long baseline afforded when combining its astrometry with that of HIPPARCOS, leading to substantial curvature in the orbit and thus a large $\dot{\mu}$. Continued observations with \textit{Gaia}, further high-contrast imaging, and RV monitoring are also likely for even better constrained orbit and dynamical mass.

The presented results provide indications for promising future directions in exoplanet characterisation. The atmosphere and brightness of GJ 758B are broadly equivalent to giant planets at younger ages of a few tens or hundreds of millions of years [Baraffe et al. 2003]. Such planets are already potentially detectable with direct imaging, and with the increased time baseline and better precision of the eventual full \textit{Gaia} release, sensitivity to such masses will also be readily provided for large numbers of targets. Therefore, our ability to simultaneously constrain the atmospheric and physical properties of wide-planet and brown dwarf companions will substantially increase in the coming years through the combination of high-contrast imaging and astrometric data as combined in this study.

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