Near-field strong coupling of single quantum dots

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Strong coupling and the resultant mixing of light and matter states is an important asset for future quantum technologies. We demonstrate deterministic room temperature strong coupling of a mesoscopic colloidal quantum dot to a plasmonic nanoresonator at the apex of a scanning probe. Enormous Rabi splittings of up to 110 meV are accomplished by nanometer-precise positioning of the quantum dot with respect to the nanoresonator probe. We find that, in addition to a small mode volume of the nanoresonator, collective coherent coupling of quantum dot band-edge states and near-field proximity interaction are vital ingredients for the realization of near-field strong coupling of mesoscopic quantum dots. The broadband nature of the interaction paves the road toward ultrafast coherent manipulation of the coupled quantum dot-plasmon system under ambient conditions.

INTRODUCTION

Strong coupling (SC) of light and matter occurs if photons stored in a cavity with mode volume \( V \) and quality factor \( Q \) are repeatedly exchanged with electronic excitations in matter. Under these conditions, light and matter give up their separate identities and new dressed states arise, which modulate the response of the system to external stimuli depending on the coupling strength and photon number. To achieve SC with \( n \) emitters, the interaction rate \( g \propto \sqrt{n/V} \) needs to exceed the cavity loss rate \( \kappa \propto 1/Q \) and the total emitter decay rate \( \Gamma \). Yet, SC of only a single quantum emitter to a cavity mode is of particular interest because it results in single-photon nonlinearities for quantum gates (1) and efficient single-photon sources (2). In high-\( Q \) cavities, this single-emitter SC has successfully been achieved, but only at cryogenic temperatures by coupling to single-emitter zero-phonon lines (3). Conversely, by reducing the mode volume in plasmonic resonators and by using large numbers of emitters, SC has also been achieved at room temperature (4–9), with recent experiments reaching the single-emitter limit (10, 11).

Here, we demonstrate tunable SC of a single colloidal semiconductor quantum dot (QD) and a broadband plasmonic nanoresonator (PNR) at room temperature. We use a slit-like PNR fabricated at a corner of a single-crystal gold flake (fig. S1), which serves as a scanning probe (Fig. 1A). Nanometer-precise raster scanning of these probes across a sample containing single colloidal QDs allows us to precisely tune and optimize the coupling strength and to measure the corresponding intriguing changes in the fluorescence spectrum due to SC (see Fig. 1A, insets).

According to the standard theory (12), the coupling rate of a point dipole emitter and a resonator mode is defined as

\[
g(r) = \mu \cdot E_0(r)/\hbar
d\tag{1}
\]

where \( \mu \) is the dipole moment of the emitter and \( E_0(r) \) is the mode’s vacuum field, evaluated at the emitter position \( r \). In Eq. 1, the mode field and the emitter’s dipole moment are assumed to be independent properties of the cavity and the emitter, respectively. This assumption is perfectly valid for systems whose characteristic length scales are larger or comparable to the photon wavelength. However, coupling of emitters to subwavelength localized plasmonic modes, known to enhance local electromagnetic fields at optical frequencies, inevitably entails close proximity of the emitter and resonator, which will lead to near-field effects such as image and influential charging due to Coulomb interactions (near-field proximity effect). As we will show in this work, Eq. 1 is therefore expected to underestimate the actual value of \( g \) but is still useful to guide the experiments.

The PNR’s particular shape was chosen for three reasons. (i) The resonant modes (see instantaneous charge distribution in Fig. 1B) have multipolar character, giving rise to reduced radiative losses with \( Q \) factors as high as 30 (fig. S4), corresponding to comparatively low decay rates of 13 THz (13). Photons emitted to the far field by the slit resonator are strongly polarized (13) along the transverse axis of the resonator. (ii) A gap mode is sustained even for very narrow gaps down to the subnanometer range (14). Because the gap width is reduced, the mode energy is increasingly localized in the dielectric gap rather than in the gold (15), whereas radiation is further suppressed. (iii) The open end of the slit resonator is an ideal location to position an emitter because here the modal field distribution leaks out of the enclosed space of the slit resonator in ways similar to scanning near-field optical microscopy probes.

RESULTS

We apply scanning probe technology to reliably and repeatedly position single QDs with nanometer precision beneath the slit opening (16). The coupling strength of a single quantum emitter to the resonator mode can therefore be varied dynamically and reversibly by changing the position of the QD with respect to the PNR. We investigate colloidal CdSeTe/ZnS nanocrystals (QD800, Thermo Fisher Scientific Inc.) with an average emission wavelength of 800 nm dispersed on a glass coverslip and embedded in a 10-nm-thin polymethyl methacrylate (PMMA) film (Supplementary Materials). Before coupling with a PNR, we verify that the isolated emitter is a single QD by confirming that the intensity autocorrelation \( g^2(0) \) is below 0.5 (Fig. 2A). Figure 2B shows a photoluminescence (PL) map obtained by scanning a single QD beneath the PNR (fig. S14) within the focus of an inverted confocal microscope (\( \lambda_{\text{exc}} = 532 \) nm, excitation rate \( \Lambda = 10 \) MHz; fig. S3). Because of a slight asymmetry in the position of the slit at the probe apex or possibly a small overall tilt of the probe, only one of the tines contributes significantly to the near-field intensity enhancement, resulting in a single localized enhancement spot. The telegraphic on/off behavior, as

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the scan image is recorded line by line, provides further proof for the coupling of a single QD to the PNR (17, 18). The broad diffraction-limited background in Fig. 2B is dominated by an intense 60-nm-wide peak. Figure 2C shows a vertical line cut of the PL map (yellow open circles) at the peak position indicated by two arrows. Because the excitation rate (10 MHz in this measurement) is below the saturation rate, the increase of the absorption cross section in the presence of the probe dominates the fluorescence enhancement and the shape of the line cut (fig. S12). We investigate the coupling with the PNR and the occurrence of SC by recording emission spectra as a function of the QD’s position with respect to the PNR, as indicated by the white circles in Fig. 2B. To ensure that the drift of the tip between the recording of the PL map and the spectra is negligible during this process, we compare the intensity of the integrated spectra (blue line) with the spectrally integrated PL map and observe good agreement. Next, we analyze the particular shapes of the spectra because they reveal the coupling between the electronic states of the QD and the PNR. Figure 2D displays the recorded spectra, which have been normalized for better comparison. For large QD probe separations, the shape of the spectrum matches the fluorescence spectrum of a weakly coupled system. With increasing coupling strength, we observe pronounced changes of the emission spectrum of the coupled system. At the position of maximum resonant field strength, we discern a transition into the SC regime, but contrary to the characteristic two-peak splitting of conventional SC, an unexpected appearance of four peaks is observed. When the PNR is moved further away from the QD, the coupling strength decreases and the spectrum transforms back to that of a weakly coupled QD, signifying a truly reversible and controllable process.

We now show that the appearance of four peaks can be attributed to the charged and neutral QD states, which both couple strongly with the PNR, therefore contributing a Rabi doublet each. On the first glance, it is tempting to interpret the two doublets appearing jointly as signatures of the first and second rung of the Jaynes-Cummings ladder. However, because the interplay of excitation, coupling, and loss rates in our experiment are prohibitive for populating higher photon states, the two doublets must relate to the SC of the PNR mode to different QD states. This is possible because, in contrast to high-Q resonators with very narrow resonances, a “broadband” PNR with a 78-meV bandwidth can coherently cover multiple exciton resonances, giving rise to simultaneous probing of both QD charge states (19). The QD has a diameter of about 8 nm, leading to a small energy separation of less than 20 meV between the neutral exciton and the charged exciton (20). Charge carrier trapping of hot electrons upon incoherent excitation is a common process in QDs, leaving behind a positively charged nanocrystal core (21–25). Typically, however, this charged exciton (trion) is optically dark due to highly efficient nonradiative Auger decay (18, 26). Yet, here, SC via plasmons provides a radiative decay channel, which is significantly faster than the Auger processes, rendering the charged trion state optically active (27). Consequently, the QD states involved in the spectral response are the neutral and positively charged QD (trion) states (17). Because in general an additional charge in the QD causes increased electron-hole interaction leading to a reduced wave function overlap (28), we assign the neutral state to the outer Rabi doublet and the charged state to the inner one. The relative Rabi splitting of both states is a direct measure of the relative magnitude of the involved total transition dipole moments. We also note that recent dark-field spectroscopy experiments on QDs in bowtie nanoantenna gaps did not show four peaks (11). We ascribe this behavior to the resonant excitation via the antenna and the resulting absence of hot electrons as the main source of charging events at low excitation rates.

A simple coupled oscillator model is sufficient to predict plasmon-exciton hybridization on a semiclassical level but does not allow the calculation of emission spectra without an (artificial) addition of stochastic noise terms. Thus, to explain the measured spectra, we formulate a quantum optical model based on the Lindblad master equation. Our model describes the interaction of a quantum emitter represented as a five-level quantum system with a broadband cavity to capture
Fig. 2. Separation-dependent coupling strength. (A) Second-order autocorrelation of the photons emitted by a single QD in the absence of the probe. (B) PL map of the QD scanned beneath a PNR. The white circles indicate the positions in which the spectra have been recorded. Scale bar, 100 nm. (C) Open yellow circles: Normalized line cut of the PL map in (B) (arrow). Full blue circles: Integrated spectral amplitude recorded at the positions indicated by white circles in (B). Red circles: Coupling strength (right axis) used to model the SC spectra in (D). Gray lines: Normalized spectra recorded for different coupling strengths. Solid lines: Spectra obtained from the quantum optical model with contribution of neutral state (blue) and charged state (red).

The essentials transitions of neutral and charged QD states (two levels each) and a multiple charged state (single level; fig. S15). The evolution of the density matrix \( \rho \) is given by

\[
\rho = -i[H_1, \rho] + \frac{1}{2} \sum_k (2L_k \rho L_k^\dagger - L_k^\dagger L_k \rho - \rho L_k^\dagger L_k)
\]

where the Hamiltonian \( H_1 \) describes the coherent interaction of the cavity with two transitions in the QD (see the Supplementary Materials for details). With the jump operators \( L_k \), we take into account all incoherent processes including pumping, dephasing, radiative and non-radiative decay, and population transfer between neutral and charged QD states. Because most of the photons emitted from the strongly coupled system reach the far field via the cavity, the emission spectra are calculated via

\[
S(\omega) \propto 2 \text{Re} \left( \int_0^{\infty} a^\dagger(\tau) a(0) e^{-i\omega \tau} d\tau \right)
\]

where \( a \) is the annihilation operator of the cavity mode. The calculated spectra are shown in Fig. 2D (solid lines), in direct comparison with measured data, and reveal a coupling strength of 110 and 44 meV for the neutral \( (g_n) \) and charged \( (g_c) \) exciton, respectively, resulting in a coupling strength ratio \( g_c/g_n \) of 0.4.

The coupling strength \( g_c \), extracted from a best fit to the experimental spectra, is plotted for each QD-PNR separation in Fig. 2C (red dots). We observe that the three spectra with the highest coupling strength are recorded close to the QD emission peak. The spectrum with the highest coupling strength exhibits a comparably small emission intensity, an effect caused by the spatial displacement of the near-field intensity maxima of the nonresonant excitation field (532 nm) and the resonant mode field (800 nm) at the tip apex of the PNR (fig. S8).

The model correctly describes the experimental data in the SC regime, where coherent light-matter quantum dynamics are dominant and allow the reproduction of the shape and intensities of all four peaks. However, when extended to the weak coupling regime, it tends to underestimate the width of the spectral features. This is not surprising because modeling a QD as a five-level quantum emitter will always simplify several intrinsic QD dynamical degrees of freedom, which are responsible for its broad emission spectrum but which do not significantly contribute to SC. Using a well-established pure dephasing model with a dephasing rate of \( \gamma_d = 160 \) fs for the QD, our quantum optical model accurately reproduces the spectra in the SC regime, where coherent coupling dominates over phononic processes. In the weak coupling regime, the emission properties of the QD are heavily affected by phonons in a way that may not be accurately described by a pure dephasing model (29). Furthermore, the spectral width can also be influenced in the experiment due to the reduced charge fluctuations induced by the presence of the metallic probe as a function of distance between QD and PNR (30, 31). We have experimentally verified the effect of tip-induced spectral narrowing independently using an unstructured gold tip (fig. S10).

Uncoupled CdSeTe/ZnS nanocrystals display a blue shift for higher excitation intensities as the contribution of biexciton emission increases (32). This spectral shift also occurs for the QDs used in the present experiment and is shown in Fig. 3A for three different excitation intensities (fig. S9). Under SC conditions, this blue shift causes an intensity-dependent detuning of the QD with respect to the PNR. Figure 3B shows a series of normalized SC spectra for increasing excitation rate (bottom to top; see fig. S17 for reversibility). The increasing detuning to higher energies causes characteristic changes of the amplitudes and shifts of the Rabi peaks. The quantum model (solid line) reproduces this behavior by changing the individual resonance energy of the neutral and charged states while keeping the cavity resonance fixed. Note that we observe a saturation in fluorescence intensity due to multicharged QD states (fig. S20). In Fig. 3C, we plot the peak energies for increasing pump rate (blue shift) for several QDs showing different tuning ranges. The red markers include the peak positions of the spectra in Fig. 3B. For comparison, we show the peak energies of the neutral and charged state (black and gray solid line, respectively) extracted from the quantum model for varying detunings (dashed line) with respect to the PNR (dotted line), demonstrating spectral anti-crossing of both QD states with the PNR spectrum—a well-known manifestation of SC.

DISCUSSION

To understand why we observe SC with QDs, which are normally not bestowed with the largest dipole matrix elements, we have to focus in more detail on the coupling mechanism between colloidal QDs and the PNR at the scanning probe apex. The coupling strength, Eq. 1, depends...
structure splitting because the plasmon resonance width an electric dipole moment of 5 Debye (Supplementary Text). However, corresponds, on the basis of the Weisskopf-Wigner approximation, to state lifetime of uncoupled QDs (Groß et al. fig. S5), as well as the emitter on the vacuum field strength and the related effective mode volume (fig. S5), as well as the emitter’s dipole moment. Regarding the dipole moment, colloidal QDs are known to exhibit a fine-structure splitting due to their crystal lattice anisotropy and electron-hole interaction, leading to eight different (partially degenerate) states near the band edge (28), with the lowest state usually being optically dark (Fig. 4A, top). The lowest optically active state \( f_{\text{bright}} \) is thermally populated and determines the optical emission properties such as the resonance energy and excited state lifetime of uncoupled QDs (33). The measured lifetime of \((58 \pm 4)\) ns corresponds, on the basis of the Weisskopf-Wigner approximation, to an electric dipole moment of 5 Debye (Supplementary Text). However, because the plasmon resonance width \( \Delta \omega \) is larger than the total fine-structure splitting \( \Delta \), it can interact with all band-edge states \( f_k \) simultaneously (Fig. 4A, bottom), some of which are also reported to exhibit larger transition oscillator strengths than \( f_{\text{bright}} \) (34, 35). As shown in the Fig. 2D measurement, the slight asymmetry of the spectra in Fig. 2D is attributed to a blue shift of the QD emission when entering the SC regime. This indicates the transition from pure emission of the lowest optically active state at the band edge to the blue-shifted effective contribution of all available states \( f_k \). In addition, the near-field intensity close to the tip shows a significant gradient of one order of magnitude over length scales of the QD dimensions. In combination with a nonspherical QD shape, the plasmonic mode is therefore expected to also couple to multipolar transitions (36–38). A quantum optical model, which incorporates a nondegenerate multilevel emitter strongly coupled with a broadband resonator (fig. S19), explains and quantifies this boost of coupling strength due to collective coupling to band-edge states. The importance of the fine structure in cavity quantum electrodynamics (cQED) experiments has been recently studied in photonic crystal cavities (39), and the boost of the coupling constant is expected to be even more effective in plasmonic cavities due to a spectral width that is orders of magnitude larger. Our quantum model shows that the coupling strength is effectively tripled by collective coupling of eight active transitions at the band edge, veritably revealing the full potential of colloidal QDs as excitonic material for strong light-matter interaction.

In addition to the QD dipole moment, the evaluation of the vacuum field strength also requires a thorough study. In the dipole approximation, the coupling rate as described in Eq. 1 is proportional to the vacuum field strength, which depends on the mode volume \( V_{\text{eff}}(r) \) via \( E_0(r) = \sqrt{\frac{\hbar \omega}{2eV_{\text{eff}}(r)}} \), where \( r \) is the position of the point-like emitter. We performed finite-difference time-domain simulations based on quasi-normal modes, taking into account the local field factor (40) by including a spherical semiconductor particle mimicking the QD interaction with the PNR. The resulting coupling strength map (fig. S5) shows large variations of \( g(r) \) especially in close proximity to and also inside the semiconductor particle. This observation demonstrates that because of the finitely sized QD, determination of the coupling rate in the dipole approximation via Eq. 1 is no longer applicable. It also strengthens the assumption that multipolar transitions and therefore all fine-structure states \( f_k \) are optically accessible. The occurrence of a hot spot between the semiconductor particle and the gold already indicates the importance of short-ranged influential confinement effects (41) even in the absence of a QD exciton. We therefore argue that because of a strong, distance-dependent polarization of the metal surface for resonant interaction, the resonator and the (mesoscopic) QD can no longer be treated as independent entities if the emitter is in close proximity to the PNR (Fig. 4B). This is not only important in experiments such as ours but also of general significance. Let us thus demonstrate the role of near-field proximity-enhanced coupling for a system of two coupled gold nanorods exhibiting classical mode splitting (fig. S6). We can immediately see that for larger nanorod separations, the coupling strengths can be determined according to Eq. 1 using the near field of an isolated nanorod. However, for smaller separations in the presence of influential charging, the coupling strength according to Eq. 1 underestimates the observed coupling strength determined via the observed mode splitting. The occurrence of this near-field proximity coupling consequently challenges the applicability of the standard dipolar SC formalism of cQED, which assumes that the mode field and the related effective mode volume can be...
PNR probes), then the characteristic spectral changes can be measured.

We find that if a particular PNR can achieve SC (3 of 30 emitters and exact positioning do not have to be counteracted by statistical uncertainties regarding (time-)varying properties of quantum action (influential and image charging).

**Fig. 4. Enhanced coupling of QD and PNRs due to collective coupling of band-edge states and near-field proximity effect.** (A) Diagram of energy levels of a CdSeTe/ZnS nanocrystal weakly coupled (top) and strongly coupled (bottom) to a resonator. Fine-structure splitting into bright (black lines) and dark states (gray lines). Incoherent excitation from the ground state G into a pump state P and subsequent relaxation to the band edge E. (B) Top: Sketch of the near-field distribution at the apex of the resonator (pure mode). Bottom: Strongly coupled mesoscopic emitter influences the pure mode field via near-field proximity interaction (influential and image charging).

determined independently and, in particular, in the absence of the emitter.

The experiments presented in this work highlight the ability of the scanning probe setup used in the present study to use a PNR to probe a larger number of different single QDs, offering an advantage in comparison to conventional multistep lithographic techniques (42, 43). Experimental uncertainties regarding (time-)-varying properties of quantum emitters and exact positioning do not have to be counteracted by statistical analysis. We find that if a particular PNR can achieve SC (3 of 30 PNR probes), then the characteristic spectral changes can be measured for most of the QDs. Assuredly, the SC spectra of different single QDs obtained with the same PNR exhibit a qualitatively similar behavior. Nevertheless, variations in coupling strength and detuning parameters are observed, owing to structural differences of the colloidal QDs as well as to their orientation with respect to the electric field polarization at the apex of the PNR (fig. S18). For most of the PNR probes, weak coupling was observed, which is characterized by the well-known Purcell enhancement (fig. S11). These findings underline that our system is capable of performing a characterization of single QDs via SC spectroscopy under ambient conditions.

**CONCLUSION**

We have demonstrated SC of a scanning PNR probe to a single semiconductor QD under ambient conditions. This allows us to deliberately undergo the transition into (and out of) the SC regime for any chosen QD in range. A hierarchy of quantum models accurately predicts the SC dynamics and the resulting spectral response. Detailed analysis of the plasmonic field and the electronic structure of the semiconductor nano-
crystal challenges the current understanding of SC. In particular, we identify collective coupling of a band-edge multiplet of states as a novel formula to achieve single-emitter SC. We reveal that near-field proximity coupling requires a reconsideration of the direct applicability of standard SC theory in dipole approximation to PNRs.

Advances in nanofabrication, such as helium ion milling, will help to further reduce the width of the nanoslits well below 10 nm, which may lead to the development of polaritonic devices, and to eventually facilitate entering the realm of ultrastrong coupling. The direct applicability of the presented methodology to any zero-dimensional (0D), 1D, and 2D quantum system promises a vast impact on the investigation of light-matter interaction on the nanometer scale.

**MATERIALS AND METHODS**

For our measurements, we customized commercially available contact mode cantilevers by placing hexagonal single-crystalline gold flakes at the end of the cantilever. We then used focused ion beam (FIB) lithography to fabricate a PNR at one of the corners of the hexagon. This modified corner serves as the probe tip, which is used to raster scan across a surface covered with CdSeTe/ZnS QDs embedded in a thin PMMA film.

**Cantilever preparation**

In the first process step, the tip at the end of a contact mode cantilever (doped silicon and no reflective coating, Contact-G-50, NanoAndMore GmbH; see fig. S1A) is cut off via FIB milling (fig. S1B). Single-crystalline gold flakes are synthesized in solution based on a recipe by Guo et al. (44) and directly grown on a glass substrate (45). A flake (typical thickness, 60 nm) is picked up with a needle attached to a micromanipulator and placed at the end of the tipless cantilever such that one corner juts out 5 to 10 μm beyond the cantilever (fig. S1C). Next, the PNR is fabricated at the protruding corner of the flake via FIB lithography with gallium ions by performing a single line cut (fig. S1D). Consistent results can be achieved for different flake thicknesses by adjusting the ion dose. We did not observe any issues regarding gallium ion implantation because it mainly (if at all) concerns the substrate (46). Because in our case the etching takes place on a free-standing gold flake, we assume negligible gallium contamination. Subsequent large-area ion irradiation of the protruding gold flake close to the cantilever induces strain and causes the gold flake to bend down (fig. S1, E and F). This ensures that the resonator becomes the foremost part of the probe that touches the sample first (fig. S1G).

Figure S2A shows a scanning electron microscopy (SEM) image of the modified contact mode cantilever with a gold flake mounted on the back side before flake bending. The PNR location is marked by a circle. The inset (fig. S2B) displays a variety of PNRs fabricated for different scanning probes. Because the flake thickness and edge geometry are different for each flake, the PNR gap width and the overall geometry can vary. By adjusting the length of the cut, we can tune the cavity to any desired resonance wavelength. FIB milling a PNR on a free-standing gold sheet creates symmetrically rounded edges inside the resonator similar to the gap geometry observed in self-assembled gold dimers. These types of structures show excellent field confinement and small mode volumes (14). In comparison, top-down structuring on substrates always leads to asymmetric structures, which are narrow at the top and broad close to the substrate. Single-crystal gold flake features excellent mechanical elasticity and durability. In combination with the soft polymer-coated sample, PNR probes can be scanned in contact mode force...
feedback without signs of wear. Probes can be stored under ambient conditions and reused for further experiments.

**QD substrate preparation for SC experiments**

We spin-coated an aqueous solution (8 nM) of CdSeTe/ZnS QDs (QDot800 ITK Q21571MP, Thermo Fisher Scientific Inc.) on cleaned microscope coverslips (#1, Gerhard Menzel GmbH). Further spin coating of a 0.4% PMMA solution preserves the nanocrystal in a thin air-dried PMMA matrix to inhibit shell oxidation and to protect the QDs from being picked up and pushed away by the probe. We measured the height of the PMMA layer using atomic force microscopy (AFM) by scratching locally with a razor blade. The average PMMA thickness was measured to be 12 nm and completely covers the embedded CdSeTe/ZnS QDs. At the same time, a QD diameter of about 8 to 11 nm ensures a minimum distance between the PNR and the emitter. We found the QDs to be highly stable over a period of at least 3 months. Comparison with a fresh sample did not show any difference of the optical performance. SEM images of the QDs (for SEM purposes prepared on a conducting substrate) are displayed in Fig. S2C and confirm the size and shape distribution observed in previous transmission electron microscopy studies (47, 48).

**Optical setup**

Figure S3 sketches the optical setup. We used a continuous-wave laser diode (frequency-doubled Nd:YAG) with an emission wavelength of 532 nm to illuminate the sample via a beam splitter (ratio, 50:50) and a high numerical aperture (NA) objective (Plan APO TIRF 100×, NA 1.45, Nikon). The AFM (Bioscope, Bruker) is mounted on a customized stage on top of the sample holder stage. A 720-nm low-pass (LP) filter is used to filter the fluorescence light and to suppress the light of the broad AFM deflection laser (685 nm). To further reduce any residual light of the excitation laser, we used an additional 540-nm LP filter. The fluorescence light passes a beam splitter (ratio, 90:10), in which 90% of the transmitted light is focused via a lens (f = 300 mm) on the entrance slit of a spectrometer (Acton SpectraPro 2300i, 300 lines/mm), where it is detected by a Peltier-cooled charge-coupled device camera (Andor DU-401A BR-DD). The remaining 10% of the light is directed to a polarizing beam splitter, resulting into two orthogonally polarized beam paths, which are detected individually by two single-photon counting modules (SPCM-AQR, Perkin and Elmer). Exchanging the polarizing beam splitter with a nonpolarizing beam splitter allows us to perform Hanbury-Brown and Twiss autocorrelation measurements.

**SUPPLEMENTARY MATERIALS**

Supplementary material for this article is available at http://advances.sciencemag.org/cgi/content/full/4/eaar4906/DC1

Supplementary Text

fig. S1. Scanning probe fabrication.
fig. S2. SEM characterization.
fig. S3. Schematic of the optical setup.
fig. S4. Simulated mode profiles and far-field spectra of PNRs for different gap widths and slit lengths between 80 and 440 nm.
fig. S5. Calculating the coupling strength.
fig. S6. Near-field proximity coupling.
fig. S7. Purcell factor of PNR.
fig. S8. Emission and excitation near-field distribution.
fig. S9. QD resonance shift for high excitation rates.
fig. S10. Coupling of a QD to an unstructured gold tip.
fig. S11. Weak coupling PNR scanning probe.
fig. S12. Difference between excitation and emission enhancement.

fig. S13. Calculated fluorescence peaks for different excitation rates for an emitter scanned through a Gaussian field profile with a Purcell factor reaching up to 1000.
fig. S14. Cavity characterization.
fig. S15. Five-level diagram of the QD.
fig. S16. Decomposing the emission of a strongly coupled QD.
fig. S17. Reversible blue shift for increased excitation rates during SC.
fig. S18. Collection of spectra of five different QDs in SC with the PNR.
fig. S19. Collective coupling of a multilevel emitter with a resonant cavity.
fig. S20. Saturation of the strongly coupled system.

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