Simulation of Electron Diffusion Coefficient Interpretation on the Optimum Thickness of TiO$_2$ Photoanode in Dye-Sensitized Solar Cell (DSSC)

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Abstract. DSSC is a natural dye-based organic solar cell composed of layers of semiconductor (photoanode), dye, electrolyte, and the counter electrode. The photoanode layer on DSSC acts as a dye binder and can pass on excited electrons to the electrode counter. This component is one of the keys to improve the DSSC performance. The TiO$_2$ material has been used widely as a photoanode due to its high stability to light so that at its optimum thickness it can pass well the sunlight energy on the surface of the DSSC. When the sunlight energy impinges to DSSC for relatively long time, it can increase the working temperature. Theoretically, the increase in the working temperature of the DSSC causes an increase in the electron diffusion coefficient in the DSSC, thus affecting its performance. Therefore, the interpretation of an increase in the electron diffusion coefficient due to an increase in the thickness and working temperature in DSSC is essential to be studied. In this article, a simulation of the determination of the optimum thickness of TiO$_2$ photoanode was carried out. We studied the effect of electron diffusion coefficient on the DSSC open voltage at the optimum thickness. The highest electron diffusion coefficient in this simulation was $9.65 \times 10^{-3}$ cm$^2$/s with current density of 0.0145 A/cm$^2$, voltage of 0.3411 V, power of 0.0020 V·A/cm$^2$, and efficiency of 2.000%. We found that the higher the electron diffusion coefficient, the open voltage of DSSC increased so that its performance also increased.

Keywords: Thickness of TiO$_2$ photoanode, working temperature, electron diffusion coefficient, DSSC performance

1. Introduction
Increasing population in the world causes greater world energy demand [1]. So far, the world energy needs have been supplied by conventional energy sourced from coal, petroleum, and natural gas. This conventional energy has brought great progress in the economic field but its excessive use can damage the environment and human health [2]. This condition triggers the idea to utilize the potential of alternative energy as a substitute for conventional energy because the use of alternative energy can be one solution to overcome the problem of environmental damage [3]. Some alternative energy sources that can be utilized include biomass, wind, solar light, hydropower, and geothermal [2,4]. From some of
these alternative energy sources, sunlight energy is one of the choices and solutions to depleting fossil energy sources because the amount of energy supplied by the sun to the earth is very abundant, reaching nearly four million annually [5]. This solar light energy is basically can be converted into electrical energy using a device that is a solar panel. Based on its function, solar panel devices are often referred to as photovoltaic cells (PV cells). Initially, the developed PV cells were made from monocrystalline or polycrystalline silicon (Si) [6].

Si is one of the first intrinsic semiconductor materials applied in the manufacture of PV cells with the advantage of having high-efficiency so that the first generation of silicon cell technology is based on silicon. Furthermore, second generation solar cell technology with a thin film based on organic semiconductors was developed, and the third generation developed natural dye-based dye solar cells known as dye-sensitized solar cells (DSSC) [7].

DSSC utilizes semiconductor materials used as dye binders. One of the semiconductor materials that widely be used is titanium dioxide (TiO$_2$) [8,9]. TiO$_2$ is a semiconductor material that has unique properties including high stability against light [10] and wide energy bandgap (3.2 eV) [11]. TiO$_2$ shows a high stability under light and can be used to pass on the excited electrons toward the counter electrode.

The study of micrometer scale of DSSC modeling electrode with various thicknesses has been conducted to find the maximum power generated by the solar window [11]. In 2011, the calculation of DSSC parameters had been reported [12]. Furthermore, in 2016 an experimental study was carried out on the effect of the thickness of the micrometer on TiO$_2$ transparent working electrodes as a DSSC application [7]. An experiment of various thicknesses was reported previously on TiO$_2$ as a photoanode of DSSC [13] while a mathematical modeling had been carried out to describe an array of PV cells connected with a variable resistor [14]. Furthermore, an effect of extreme temperatures on the performance of DSSC was also reported [15].

Based on these studies, the thickness of TiO$_2$ photoanodes and the effect of working temperature are the key to improving DSSC performance. The longer time of DSSC to be exposed under sunlight, the working temperature will increase. Theoretically, the increase in working temperature affects the increasing in diffusion coefficient of the electron [16]. This subsequently affects the performance of DSSC. Therefore, in addition to the thickness optimization of TiO$_2$ photoanode, the effect of increasing the electron diffusion coefficient on DSSC due to the increase in work temperature needs to be studied.

2. Methods

In this study, the simulation was carried out to obtain the optimum thickness of TiO$_2$ photoanode. This optimum thickness could be analyzed based on the results of the electrical current to the electrical voltage (J-V) and the electrical power to the electrical voltage (P-V) curves. The simulated thickness was in the range of 1 nm to 20 µm. The simulation activities were conducted using the appropriate input parameters in Table 1.

| Parameter | Value | Remarks | Reference |
|-----------|-------|---------|-----------|
| $k$       | 1.381x10$^{-23}$ J/K | Boltzmann constant | [12] |
| $q$       | 1.602 x10$^{-19}$ C | electron charge | |
| $L$       | 2.2361 x10$^{-3}$ cm | length of electron diffusion | |
| $\alpha$  | 5000 cm$^{-1}$ | absorption coefficient | [9, 12] |
| $m$       | 4.5 | ideal factor | [9,11,12] |
| $D$       | 2.3x10$^{-4}$ cm$^2$/s | diffusion coefficient | [9] |
| $n_0$     | 10$^{16}$ elektron/cm$^3$ | electron concentration | [9,11,12] |
| $\tau$    | 0.01 s | lifetime | [9, 11,12] |
| $\phi$    | 1x10$^{17}$ cm$^{-2}$s$^{-1}$ | sunlight intensity | [9, 11] |
| $\mu$     | 0.3 cm$^2$/Vs | electron mobility | [9] |
After obtaining the optimum thickness of TiO$_2$ photoanode, the variations in electron diffusion coefficient values were made due to work temperature changes that may occur when DSSC was exposed to the sunlight. Then, the increase in the electron diffusion coefficient value was connected graphically to the voltage value generated by the DSSC, so that the graph (D-V) was obtained. This simulation was conducted by solving the mathematical equations in DSSC, which were the Equation (1) for the value of the electric current, Equation (2) for the voltage, Equation (3) for the efficiency value of DSSC, and Equation (4) for calculating electron diffusion coefficient [9,11]:

$$J_{sc} = \frac{q\phi L\alpha}{1 - \frac{L^2}{\alpha^2}} \left[ -L\alpha + \tanh \left( \frac{d}{L} \right) + \frac{L\alpha \exp(-d\alpha)}{\cosh \left( \frac{d}{L} \right)} \right]$$

$$V_{oc} = \frac{kTm}{q} \ln \left[ \frac{L(J_{sc} - J)}{qDn_0 \tanh \left( \frac{d}{L} \right)} + 1 \right]$$

$$\eta = \frac{P_{max}}{P_{in}} \times 100\%$$

$$D = \frac{kT\mu}{q}$$

3. Results and Discussion
The completion of Equation (1) through Equation (3) in a simulation could produce a relationship between electric current vs. electrical voltage (J-V) and maximum electrical power vs. open voltage (P-V) curves on various TiO$_2$ thicknesses. The typical results are shown in Figure 1 and Figure 2. The purpose was to obtain the optimum thickness of TiO$_2$ photoanode because in this state, TiO$_2$ could properly pass solar light energy into the DSSC. This could be proven by the $J_{sc}$, $V_{oc}$, and $P_{max}$ as written in Table 2.

![Figure 1. DSSC J-V curve on various thicknesses of TiO$_2$ photoanode (d)](image1)

![Figure 2. DSSC P-V curve on different thickness variations of TiO$_2$ photoanode (d)](image2)
The determination of the optimum thickness of TiO₂ photoanode was analyzed based on Figure 1, Figure 2, and Table 2. In Figure 1, the optimum current density in the TiO₂ thickness was 5 µm and 10 µm. Meanwhile, Figure 2 is a result showing the maximum power ($P_{max}$) ascribed by the peaks. The highest was achieved by the sample with the thickness of 5 µm. This can be seen in Table 2, the highest $P_{max}$ was 0.0049 V·A/cm².

Table 2. Simulation results at the different thicknesses (d) at 300 K

| d  | $J_{sc}$ (A/cm²) | $V_{oc}$ (Volt) | $P_{max}$ (Volt A/cm²) | $\eta$ (%) |
|----|-----------------|----------------|------------------------|------------|
| 1 nm | 8.0080 x 10⁻⁶ | 0.7234 | 3.4469 x 10⁻⁶ | 0.0034 |
| 300 nm | 0.0022 | 0.7149 | 0.0009 | 0.9448 |
| 600 nm | 0.0042 | 0.7065 | 0.0017 | 1.700 |
| 900 nm | 0.0058 | 0.6983 | 0.0024 | 2.400 |
| 1 µm | 0.0063 | 0.6957 | 0.0026 | 2.600 |
| 5 µm | 0.0145 | 0.6079 | 0.0049 | 4.900 |
| 10 µm | 0.0154 | 0.5402 | 0.0044 | 4.400 |
| 15 µm | 0.0153 | 0.5008 | 0.0039 | 3.900 |
| 20 µm | 0.0151 | 0.4768 | 0.0036 | 3.600 |

Based on the simulation results, it is shown that the P-V curve was like a parabolic graph due to the occurrence of processes in the DSSC namely the generation of recombination of charge carriers, especially electrons in a certain time span (lifetime). $P_{max}$ is the peak point on the P-V curve which is the limit of the change of electron generation events to recombination. The existence of these events caused an electrical phenomenon when DSSC was exposed to the sunlight. At a thickness of 5 µm, the highest efficiency ($\eta$) and increase in the current density ($J_{sc}$) were obtained. Based on these data, it is known that the thickness of TiO₂ photoanode had an important role in accordance with the research of Ni et al. [11] that the thickness of TiO₂ gave a change in the performance of DSSC.

By obtaining the optimum thickness, we further analyzed other factors such as working temperature associated with the length of time DSSC exposed under the sunlight. By implementing Equation (4), we found that the working temperature affected the electrical parameters in the DSSC namely electron diffusion coefficient ($D$). By assuming TiO₂ electron mobility was constant of 0.3 cm²/V·s [17], the working temperature (T) and the electron diffusion coefficient ($D$) increased as well. This relationship is illustrated in Figure 3.

Figure 3. The graph of electron diffusion coefficients vs. voltage of DSSC (D-V) for the sample with a thickness of TiO₂ (5 µm)
The simulated electron coefficient diffusion \((D)\) was obtained with analytical calculations based on the equation (4) at working temperature of 273 K to 373 K. The DSSC parameters inferred from Figure 3 and Equation (4) are listed in Table 3.

**Table 3. Simulation results of electron diffusion coefficient \((D)\) at an optimum thickness (5 µm)**

| \(D\) (cm\(^2\)/s) | \(\ J_e\) (A/cm\(^2\)) | \(V_{oc}\) (Volt) | \(P_{max}\) (Volt A/cm\(^2\)) | \(\eta\) (%) |
|----------------|------------------------|-----------------|-------------------------|----------|
| 7.06 x 10\(^{-3}\) | 0.0145 | 0.2800 | 0.0017 | 1.700 |
| 7.32 x 10\(^{-3}\) | 0.0145 | 0.2866 | 0.0018 | 1.800 |
| 7.58 x 10\(^{-3}\) | 0.0145 | 0.2930 | 0.0018 | 1.800 |
| 7.84 x 10\(^{-3}\) | 0.0145 | 0.2994 | 0.0018 | 1.800 |
| 8.09 x 10\(^{-3}\) | 0.0145 | 0.3057 | 0.0018 | 1.800 |
| 8.36 x 10\(^{-3}\) | 0.0145 | 0.3117 | 0.0019 | 1.900 |
| 8.62 x 10\(^{-3}\) | 0.0145 | 0.3178 | 0.0019 | 1.900 |
| 8.87 x 10\(^{-3}\) | 0.0145 | 0.3238 | 0.0019 | 1.900 |
| 9.13 x 10\(^{-3}\) | 0.0145 | 0.3297 | 0.0020 | 2.000 |
| 9.39 x 10\(^{-3}\) | 0.0145 | 0.3354 | 0.0020 | 2.000 |
| 9.65 x 10\(^{-3}\) | 0.0145 | 0.3411 | 0.0020 | 2.000 |

From Table 3, we found that the highest electrical parameter of DSSC was at the most considerable electron diffusion coefficient \(9.65 \times 10^{-3}\) cm\(^2\)/s. This result is in accordance with the research of Ni et al. [11]. Ni et al. [11] reported that the changes in the electron diffusion coefficient were strongly affected by the TiO\(_2\) thickness at room temperature (300 K). In the case of DSSC when exposed at a relatively long time, it may cause the working temperature of DSSC to increase more than room temperature (300 K). At the optimum thickness of TiO\(_2\), one of the parameters that change due to the increase in the working temperature of the DSSC is the electron diffusion coefficient. The results obtained from this study are written in Table 3 and Figure 3 showing the greater the working temperature, the greater the electron diffusion coefficient. The electron diffusion coefficient affects the open voltage \(V_{oc}\), maximum power \(P_{max}\), and its efficiency \(\eta\). An empirical work of various metal oxides may be found in recent works [18,19] and references therein.

On the other hand, the changes of the electron diffusion coefficient do not sufficiently affect the current density \(J_{oc}\). This result occurred because the \(J_{oc}\) is significantly dependent on sunlight intensity on the surface of the DSSC. The intensity of sunlight was assumed to be constant at \(100\) mW/cm\(^2\) or \(1\times10^{17}\) cm\(^2\)/s\(^{-1}\) corresponds to Table 1. In addition, the difference in the electron diffusion coefficients between the simulated data was quite small due to the weak change in DSSC working temperature [12]. This condition proves that a weak change in the electron diffusion coefficient is not significant effect on the current density of DSSC. Physically, the diffusion coefficient reflects how big the gradient/difference in electron concentration. So, in general, the greater electron diffusion coefficient can affect the voltage generated by DSSC. There are many reports associated with the current study. The trend is closely similar with different optimum and also slightly different features. Several related solar cell parameters could be also considered. A relative rigor inferential work on various solar cell parameter fittings is recently reported [20].

**4. Conclusion**

By the simulation method, we found that the optimum thickness of TiO\(_2\) DSSC photoanode was 5 µm. At the optimum thickness of TiO\(_2\) photoanode, it was shown that the higher electron diffusion coefficient \((D)\), the open voltage increased \(V_{oc}\). The highest electron diffusion coefficient of \(9.65 \times 10^{-3}\) cm\(^2\)/s and the working temperature of 373 K produced a maximum power of \(P_{max} = 0.0020\) V\(\cdot\)A/cm\(^2\) and open voltage of \(V_{oc} = 0.3411\) V.
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