No strong dependence of Lyman continuum leakage on physical properties of star-forming galaxies at $3.1 \lesssim z \lesssim 3.5$

A. Saxena, L. Pentericci, R. S. Ellis, L. Guaita, A. Calabrò, D. Schaerer, E. Vanzella, R. Amorín, M. Bolzonella, M. Castellano, F. Fontanot, N. P. Hathi, P. Hibon, M. Llerena, F. Mannucci, A. Saldana-Lopez, M. Talia, G. Zamorani

1 Department of Physics and Astronomy, University College London, Gower Street, London WC1E 6BT, UK
2 INAF – Osservatorio Astronomico di Roma, via Frascati 33, 00078, Monteporzio Catone, Italy
3 Departamento de Ciencias Físicas, Universidad Andres Bello, Fernandez Concha 700, Las Condes, Santiago, Chile
4 Observatoire de Genève, Département d’Astronomie, Université de Genève, 51 Chemin Pegasi, 1290 Versoix, Switzerland
5 CNRS, IPAR, 14 avenue E. Bellin, 31400 Toulouse, France
6 INAF – Osservatorio Astronomico di Bologna, Via P. Gobetti 93/3, 40129 Bologna, Italy
7 Instituto de Investigación Multidisciplinar en Ciencia y Tecnología, Universidad de La Serena, Raúl Bitrán, 1305 La Serena, Chile
8 Departamento de Física y Astronomía, Universidad de La Serena, Av. Juan Cisternas 1200 Norte, La Serena, Chile
9 INAF - Osservatorio Astrofisico di Arcetri, Largo E. Fermi 5, 50125 Firenze, Italy
10 INAF – Astronomical Observatory of Trieste, Via G.B. Tiepolo 11, 34143 Trieste, Italy
11 IFPU — Institute for Fundamental Physics of the Universe, Via Beirut 2, 34151 Trieste, Italy
12 Space Telescope Science Institute, 3700 San Martin Drive, Baltimore, MD 21218, USA
13 European Southern Observatory (ESO), Vitacura, Chile
14 INAF – Osservatorio Astrofisico di Arcetri, Largo E. Fermi 5, 50125 Firenze, Italy
15 University of Bologna – Department of Physics and Astronomy ‘Augusto Righi’ (DIFA), Via Gobetti 93/2, 40129 Bologna, Italy

Accepted 2021 December 19. Received 2021 November 23; in original form 2021 September 09

ABSTRACT

We present Lyman continuum (LyC) radiation escape fraction ($f_{\text{esc}}$) measurements for 183 spectroscopically confirmed star-forming galaxies in the redshift range $3.11 < z < 3.53$ in the Chandra Deep Field South. We use ground-based imaging to measure $f_{\text{esc}}$, and use ground- and space-based photometry to derive galaxy physical properties using spectral energy distribution (SED) fitting. We additionally derive [O III] + Hβ equivalent widths (that fall in the observed K band) by including nebular emission in SED fitting. After removing foreground contaminants, we report the discovery of 11 new candidate LyC leakers at $z \gtrsim 2 \sigma$ level, with $f_{\text{esc}}$ in the range 0.14 – 0.85. From non-detections, we place 1σ upper limits of $f_{\text{esc}} < 0.12$, where the Lyman-break selected galaxies have $f_{\text{esc}} < 0.11$ and ‘blindly’ discovered galaxies with no prior photometric selection have $f_{\text{esc}} < 0.13$. We find a slightly higher 1σ limit of $f_{\text{esc}} < 0.20$ from extreme emission line galaxies with rest-frame [O III] + Hβ equivalent widths $> 300$ Å. For candidate LyC leakers, we find a weak negative correlation between $f_{\text{esc}}$ and galaxy stellar masses, no correlation between $f_{\text{esc}}$ and specific star-formation rates (sSFRs) and a positive correlation between $f_{\text{esc}}$ and EW_{[O III]} + Hβ). The weak/no correlations between stellar mass and sSFRs may be explained by misaligned viewing angles and/or non-coincident timescales of starburst activity and periods of high $f_{\text{esc}}$. Alternatively, escaping radiation may predominantly occur in highly localised star-forming regions, or $f_{\text{esc}}$ measurements may be impacted by stochasticity of the intervening neutral medium, obscuring any global trends with galaxy properties. These hypotheses have important consequences for models of reionisation.

Key words: cosmology: dark ages, reionisation, first stars – cosmology: early Universe – galaxies: high-redshift – galaxies: evolution

1 INTRODUCTION

Constraining when and how the intergalactic medium (IGM) in the Universe made a phase transition from neutral to completely ionised, i.e. the epoch of reionisation (EoR) is an exciting challenge in observational cosmology. An important period in the evolutionary history of our Universe, EoR was likely triggered by UV photon production by the first stars, galaxies and supermassive black holes in the Universe (Bromm & Yoshida 2011) and observations suggest that the reionisation of the Universe unfolded over the redshift range $6 \lesssim z \lesssim 10$ (e.g. Planck Collaboration et al. 2016b). To understand how reionisation progressed, knowledge of the intrinsic ionising spectra of sources in the early Universe is needed, in addition to the fraction of Hydrogen-ionising Lyman continuum (LyC; $\lambda_0 < 912$ Å) photons that actually escape into the neutral IGM driv-
...ing reionisation (see Dayal & Ferrara 2018, for a recent review). The rapidly increasing neutrality of the IGM at high redshifts (e.g. Inoue et al. 2014) makes it impossible to directly observe LyC photons from reionisation era galaxies even with facilities like the James Webb Space Telescope (JWST) and therefore, the only possibility to obtain constraints on the escape fraction of LyC photons ($f_{\text{esc}}$) is by studying lower redshift analogues of reionisation era galaxies, where escaping LyC photons are not completely absorbed by the comparatively less neutral IGM.

Assuming a constant LyC escape fraction for galaxies across the full range of UV luminosities or stellar masses, various works (Robertson et al. 2013, 2015, but see also Naidu et al. 2020) have determined that $f_{\text{esc}} \approx 10 \pm 20\%$ required to both reionise the Universe by $z \approx 6$ and match the Thomson optical depth of electron scattering observed in the cosmic microwave background (Planck Collaboration et al. 2016b). High-resolution zoom-in simulations of reionisation era galaxies have suggested that $f_{\text{esc}}$ could be higher in lower mass systems, as the energy and momentum ejected by supernova explosions are able to clear out channels of neutral gas more efficiently in lower mass environments, facilitating LyC photon escape (Wise et al. 2014; Trebitsch et al. 2017). Other simulations, however, have suggested a non-monotonic dependence of $f_{\text{esc}}$ on stellar/halo mass, where $f_{\text{esc}}$ is lower at the low mass end ($M_* < 10^8 M_\odot$) due to inefficient star formation, peaks at $M_* \approx 10^9 M_\odot$ and decreases again at higher masses due to dust attenuation (e.g. Ma et al. 2020).

Alternatively, a strong dependence of $f_{\text{esc}}$ on the star-formation rate surface density may imply that higher mass galaxies ($>10^8 M_\odot$) at $z > 6$ may contribute $>80\%$ of the reionisation photon budget and also explain the rapid conclusion of reionisation (Naidu et al. 2020). Active galactic nuclei (AGN) at $z > 6$, with a considerably higher $f_{\text{esc}}$ on average compared to star-forming galaxies (Cristiani et al. 2016; Grazian et al. 2018; Romano et al. 2019), may also contribute to the observed rapid evolution of the IGM neutral fraction at $z > 6$ (Fontanot et al. 2012; Giallongo et al. 2015; Trebitsch et al. 2018; Finkelstein et al. 2019; Dayal et al. 2020), and contributions to the reionisation epoch may be expected from low-metallicity X-ray binaries binary populations in high redshift galaxies (Madau & Fragos 2017; Schauer et al. 2019; Saxena et al. 2021).

However, no conclusive correlations between $f_{\text{esc}}$ and stellar masses or star-formation rates have yet been identified observationally. LyC measurements presented by Izotov et al. (2021) for a sample of very low mass ($M_* < 10^8 M_\odot$) galaxies at $0.30 < z < 0.45$ showed that $f_{\text{esc}}$ does not strongly depend on the stellar mass over a broad mass range of $10^7 - 10^{10} M_\odot$. Radiative transfer modelling has suggested that density-bounded H ii regions within star-forming galaxies, traced by high [O iii]/[O ii] ratios (O32; Zackrisson et al. 2013), offer ideal environments to achieve high $f_{\text{esc}}$ values (Jaskot & Oey 2013; Nakajima & Ouchi 2014; Faiss 2016; Izotov et al. 2018a) and although spectroscopic follow-up of candidate LyC leakers at $z \approx 3$ has shown that galaxies with high $f_{\text{esc}}$ can also show high O32 (e.g. Vanzella et al. 2016b; Nakajima et al. 2020), several other physical phenomena that do not require high $f_{\text{esc}}$ can also lead to high O32 ratios within galaxies (e.g. Stasińska et al. 2015; Izotov et al. 2017; Paullast et al. 2018; Jaskot et al. 2019). Therefore, a high O32 does not also necessarily guarantee high $f_{\text{esc}}$ (Izotov et al. 2018a; Naidu et al. 2018; Bassett et al. 2019; Nakajima et al. 2020).

Further, studies that have attempted to measure $f_{\text{esc}}$ from intermediate redshift galaxies using both ground-based (e.g. Grazian et al. 2016; Gualia et al. 2016; Marchi et al. 2017a; Japelj et al. 2017; Naidu et al. 2018) and space-based (e.g. Siana et al. 2015; Mostardi et al. 2015; Rutkowski et al. 2017; Fletcher et al. 2019) UV imaging have generally found low $f_{\text{esc}}$ values (< 10 – 20%), with no clear differences in $f_{\text{esc}}$ measured from photometrically selected Lyman break galaxies (LBGs) or galaxies selected based on strong emission lines. LyC $f_{\text{esc}}$ measured from compact Lyman alpha emitting galaxies (LAEs), considered to be direct analogues of reionisation era galaxies, have reported a higher incidence of individual LyC leakers (with $f_{\text{esc}} \geq 10\%$; e.g. Fletcher et al. 2019), but average $f_{\text{esc}}$ measured through stacking of non-leakers remains low (Mostardi et al. 2013; Fletcher et al. 2019; Bian & Fan 2020; Smith et al. 2020) and consistent with that derived for other types of galaxies. The candidate LyC leaking galaxies identified at $z \approx 2 – 4$, with $f_{\text{esc}} > 20\%$ (e.g. de Barros et al. 2016; Vanzella et al. 2016a, 2018; Shapley et al. 2016; Bian et al. 2017; Rivera-Thorsen et al. 2019; Fletcher et al. 2019; Meštric et al. 2020; Marques-Chaves et al. 2021), also generally occupy a broad range of stellar masses, star-formation rates and rest-optical nebular line strengths (e.g. [O iii]), showing no clear preference or dependence on either of these parameters.

To fully understand the nature of galaxies that drove reionisation, thereby dictating both the spatial and temporal evolution of the neutral fraction of the IGM at $z > 6$, it is necessary to uniformly probe the dependence of $f_{\text{esc}}$ on galaxy properties using large samples of star-forming galaxies at intermediate redshifts. To do this, a combination of accurate spectroscopic redshifts, deep rest-frame LyC data and multi-band photometry that enables reliable constraints on the spectral energy distributions (SEDs) is needed. This combination is crucial to overcome uncertainties in the measurement of both LyC $f_{\text{esc}}$ as well as galaxy properties such as stellar masses, star-formation rates (SFRs), histories, ages, metallicities, dust attenuation, etc., which may also impact the inferred $f_{\text{esc}}$ (Dayal & Ferrara 2018). Accurate redshifts can also minimise the uncertainties in the IGM transmission along the line-of-sight that can further affect the $f_{\text{esc}}$ measurement (e.g. Bassett et al. 2021).

Therefore, in this study we construct a sample of star-forming galaxies with high quality spectroscopic redshifts at $z \approx 3.11 - 3.53$ for which deep ground-based imaging probing rest-frame LyC emission is available. Our aim is to uniformly measure LyC $f_{\text{esc}}$ and key galaxy properties using SED fitting to explore potential correlations between them. The galaxy sample used in this study probes a range of UV luminosities, stellar masses and star-formation rates, containing galaxies that were photometrically selected for spectroscopic follow-up based on their Lyman break, as well as blindly discovered galaxies from deep imaging-spectroscopy surveys of the sky. Each galaxy benefits from deep Hubble Space Telescope (HST) and Spitzer/IRAC imaging of their non-ionising wavelengths, which enables highly reliable SED fitting. The redshift range of our sample is further advantageous due to the redshifted [O iii] + Hβ emission lines falling in the observed K broadband, enabling the exploration of the connection between $f_{\text{esc}}$ and [O iii] + Hβ line strengths.

The layout of this paper is as follows. We describe the LyC imaging and the spectroscopic data sets used in this study, along with the sample selection and foreground contamination identification in §2. In §3 we describe the SED fitting procedure used to derive key physical properties for our galaxies as well as estimate [O iii] + Hβ line strengths. In §4 we describe our LyC $f_{\text{esc}}$ measurements and present the results for both individual galaxies as well as $f_{\text{esc}}$ measured through stacking. We also present stacked $f_{\text{esc}}$ measurements for sub-samples of galaxies, including those for galaxies that show extremely strong [O iii] + Hβ emission lines. In §5 we explore the dependence of $f_{\text{esc}}$ on key galaxy properties such as stellar masses, specific star-formation rates and [O iii] + Hβ strengths for both individual $f_{\text{esc}}$ measurements and stacks. Finally in §6 we discuss the implications of our results and discuss mechanisms that likely regulate $f_{\text{esc}}$. 

MN/RAS 000, 1–18 (2021)
Throughout this paper, we assume a ΛCDM cosmology with $\Omega_m = 0.3$ and $H_0 = 67.7 \text{ km s}^{-1} \text{ Mpc}^{-1}$ taken from Planck Collaboration et al. (2016a), and use the AB magnitude system (Oke & Gunn 1983). All logarithms are in base 10, unless otherwise specified.

2 DATA AND SAMPLE SELECTION

In this work, we focus on the Great Observatories Origins Deep Survey-South (GOODS-S) extragalactic field, which benefits from deep photometric and spectroscopic observations of galaxies from ground- and space-based observatories across a wide wavelength range, for example through the Cosmic Assembly Near-infrared Deep Extragalactic Legacy Survey (CANDELS; Grogin et al. 2011; Koekemoer et al. 2011). This field also benefits from deep narrow-band (Guaita et al. 2016) and broad-band imaging data (Nonino et al. 2009) probing rest-frame LyC wavelengths at $z \sim 3 - 3.5$, and deep HST and Spitzer data that enables reliable SED fitting, crucially at wavelengths redwards of the Balmer break at $z \sim 3.5$ (around 4000 Å rest-frame). We first describe the available LyC filters in this field below, followed by the spectroscopic data used in this study, possible foreground contaminant identification and final galaxy sample creation.

2.1 LyC filters – narrow bands and U-band

To measure LyC signal, typically measured in the rest-frame wavelength range 860 < $\lambda$ < 912 Å at $z > 3$, we use narrow-band imaging data from Guaita et al. (2016) and the publicly available U-band imaging data (Nonino et al. 2009). We briefly describe the properties of these LyC filters below.

The images from the narrow bands (NB) NB3727 and NB396 were first presented in Guaita et al. (2016) and we refer the readers to this paper for full details of the observations, data reduction, calibration and other properties associated with these images. Briefly, the NB3727 image was obtained using the MOSAIC II instrument at the Cerro Tololo Interamerican Observatory (CTIO), with the exposure time totalling to 36 hours, a total coverage area of 31.5' × 31.5' on the sky and 1σ detection limit of 27.38 AB. NB3727 offers LyC coverage in the wavelength range mentioned above for redshifts $3.11 < z < 3.34$.

The NB396 image was obtained using the WFI instrument mounted on the ESO 2.2m Telescope at La Silla, with a total exposure time of 13 hours, covering a subset of the sky area encompassed by the NB3727 image with a 1σ detection limit at 27.72 AB. NB396 samples LyC signal in the range $3.41 < z < 3.53$.

We also use the deep U-band image in the GOODS-S field taken by Nonino et al. (2009) using VIMOS on the Very Large Telescope (VLT) covering an area of $\approx 630$ arcmin$^2$ and reaching a 1σ magnitude limit of 29.78 AB. The U-band filter covers rest-frame LyC signal in the redshift range $3.34 < z < 3.49$. Although flux bluewards of the Lyman break is sampled for redshifts above 3.49, the declining IGM transmissivity would strongly suppress the expected flux at these shorter wavelengths (e.g. Inoue et al. 2014) and may bias the measured LyC fluxes. The transmission curves and the redshift range over which the rest-frame LyC flux is sampled by each filter are shown in Figure 1.

Therefore, owing to the rest-frame LyC wavelength coverage offered by imaging data, the redshift range probed in this study is $3.11 < z < 3.53$. We now present the spectroscopic data within the GOODS-S/CDFS field used to construct a sample of star-forming galaxies in this redshift range.

2.2 Spectroscopic data

2.2.1 VANDELS

The majority of spectra used in this study are from VANDELS – a deep VIMOS survey of the CANDELS UDS and CDFS fields – which is a recently completed ESO public spectroscopic survey carried out using the VLT. The VANDELS survey covers two well-studied extragalactic fields, the UKIDSS Ultra Deep Survey (UDS) centred around RA = 02:17:38, Dec = -05:11:55, and the Chandra Deep Field South (CDFS/GOODS-S) centred around RA = 03:32:30, Dec = -27:48:28. As mentioned earlier, we use VANDELS spectra in the CDFS/GOODS-S field in this study. The survey description and target selection can be found in McLaren et al. (2018), and detailed data reduction and redshift determination steps can be found in Pentericci et al. (2018).

VANDELS spectroscopic targets were selected based on photometric redshifts (or the presence of Lyman breaks in their broadband photometry) derived from deep ground and space-based multi-band photometry. The parent spectroscopic sample included bright star-forming galaxies ($i < 25.0$ AB) in the range $2.4 < z < 5.5$ with 99% of this subsample having specific star-formation rates (sSFR) > 0.6 Gyr$^{-1}$, fainter Lyman-break galaxies (LBGs; $i \leq 27.5$ AB) in the redshift range $3.0 < z \leq 7.0$ with sSFR > 0.3 Gyr$^{-1}$ and passive galaxies with sSFR < 0.1 Gyr$^{-1}$ (McLure et al. 2018). Over the redshift range of interest for this study, the VANDELS galaxies are largely sampled from the star-forming main sequence.

The latest VANDELS data release, DR4 (Garilli et al. 2021) contains spectra of $\approx 2100$ galaxies in the redshift range $1.0 < z < 7.0$, with on-source integration times ranging from 20 to 80 hours, where > 70% of the targets have at least 40 hours of integration time. The survey depths have been chosen so that the final spectra have high

---

1 https://www.stsci.edu/science/goods/

2 http://vandels.inaf.it/dr4.html
signal-to-noise ratios (SNRs), enabling detailed absorption and emission line studies, the study of ionising sources using emission line ratios, the derivation of accurate metallicities and better constraints on physical parameters such as stellar masses and star-formation rates. The spectral resolution of the final spectra is $R \sim 600$.

The spectra used in this study were reduced using the EASYLIFE data reduction pipeline (Garilli et al. 2012) and the final data products delivered by VANDELS include the extracted 1D spectra, the 2D re-sampled and sky-subtracted spectra and catalogues with physical parameters, including spectroscopic redshifts. The reliability of redshifts in the VANDELS database is recorded using the following flags: 0 – no redshift could be assigned, 1 – 50% probability to be correct, 2 – 70-80% probability to be correct, 3 – 95-100% probability to be correct and 9 – spectrum shows a single emission line. The typical accuracy of spectroscopic redshift measurements is $\sim 150 \text{ km s}^{-1}$. Details about the final VANDELS data products, redshift determination processes and redshift reliability flags assignment can be found in Pentericci et al. (2018).

In the redshift range $3.1 < z < 3.5$, we identified 90 galaxies with spectroscopic flags 3 and 4, which guarantees a $> 95\%$ probability that the spectroscopic redshift is correct and reliable. The VANDELS team has performed aperture matched, PSF-homogenised photometry for every source identified in the CANDELS footprint in GOODS-S across available imaging data ranging from UV to NIR wavelengths (McLure et al. 2018), which we refer to as the ‘master’ catalogue. Accurate and homogenised photometry is essential for robust spectral energy distribution (SED) fitting to determine key galaxy properties and we rely on photometry from this master catalogue for this study.

Therefore, moving forward we require every source selected from other publicly available spectroscopic data that are described below to have a matched entry in the master catalogue and below we list the other publicly available data sets from which sources with reliable spectroscopic redshifts were queried.

### 2.2.2 VUDS

The VIMOS Ultra-Deep Survey (VUDS; Le Fèvre et al. 2015) is a survey of $\sim 10000$ faint galaxies in the redshift range $2 < z < 6$ with $i$-band magnitudes down to $i \approx 27.0 \text{ AB}$. The spectroscopic targets were also selected based on either reliable photometric redshifts or the presence of a Lyman break (LBGs) at higher redshifts, similar to VANDELS.

From the VUDS survey, we select sources in the GOODS-S/CDFS field with redshift reliability greater than 95%, where the redshift reliability flags are determined in a similar manner to VANDELS. We refer the reader to Le Fèvre et al. (2015) and Tasca et al. (2017) for more information about source selection, data reduction and redshift measurements. In total we select 20 sources with reliable spectroscopic redshifts from VUDS.

### 2.2.3 VIMOS10

The publicly available VLT/VIMOS spectroscopic survey in GOODS-S (Balestra et al. 2010; VIMOS10) contains spectra obtained using both the Low Resolution and Medium Resolution grisms for galaxies up to $z \sim 3.5$ with $B$ and $R$ magnitudes $\sim 24-25 \text{ AB}$. The spectroscopic targets were predominantly LBGs, similar to VANDELS and VUDS. We only use sources that have ‘secure’ redshifts, i.e., $> 99\%$ confidence of being correct owing to the relatively lower integration times of this survey, and find that 43 sources satisfied our selection criteria.

### 2.2.4 MUSE-WIDE Survey

In addition to photo-z or LBG selected spectroscopic targets, we query reliable spectroscopic redshifts from the publicly available MUSE-WIDE survey in the GOODS-S/CDFS field, which is a ‘blind’ integral-field unit (IFU) survey carried out without photometric pre-selection (Urrutia et al. 2019). The unique aspect of surveys enabled by MUSE on the VLT is that no photometric pre-selection is required prior to obtaining a spectroscopic redshift. Therefore, spectroscopically confirmed sources are often blindly selected, owing to their emission lines alone and not necessarily their photometric redshifts or Lyman (or Balmer) breaks, which may bias the target selection. The MUSE-WIDE Survey is capable of obtaining spectroscopic redshifts for 98% of photometrically selected galaxies brighter than $24.0 \text{ AB} \text{ in } HST/F775W$. This blind galaxy sample is therefore highly complementary to the photo-z or LBG selection implemented by other data sets used in this study.

From this survey, we select sources with redshifts $3.1 < z < 3.5$ and reliable spectroscopic redshifts, i.e. a ‘confidence’ value of 2 or 3, corresponding to an expected error rate of $\leq 10\%$ in the correct identification of emission and absorption features (Urrutia et al. 2019). We find that 44 galaxies in the MUSE-WIDE data release satisfy our selection criteria.

### 2.2.5 MUSE-HUDF Survey

We also use the published spectroscopic redshifts from the MUSE deep (coverage area of $3' \times 3'$) and ultra deep (coverage area of $1' \times 1'$) surveys in the Hubble Ultra Deep Field (HUDF; Inami et al. 2017), which is part of the GOODS-S field. This survey is deeper than MUSE-WIDE and is capable of blindly detecting sources as faint as $\approx 30.0 \text{ AB} \text{ in } HST/F775W$ (Inami et al. 2017).

We find that 42 sources from MUSE-HUDF lie in the redshift range of interest and have reliable spectroscopic redshifts, represented by confidence levels 2 and 3 and these sources are added to our sample.

### 2.2.6 3D-HST

Additional redshifts were queried from the 3D-HST survey, which is a spectroscopic survey conducted using the WFC3/G141 as well as the ACS/G800L grisms on the $HST$ covering $\sim 600$ square arcminutes of well-studied extragalactic fields, including GOODS-S (Brammer et al. 2012; Momcheva et al. 2016). The 3D-HST survey obtained blind spectroscopy of galaxies, with the redshift determination primarily relying on the $[\text{O} \alpha]$ emission line in the redshift range of interest to this study. Since there was no photometric pre-selection required, the 3D-HST survey is similar to the MUSE surveys.

We add a further 9 sources to our study from 3D-HST that have “good” redshifts (use_subj = 1) from the publicly available catalogues.

3 http://cesam.lam.fr/vuds/

4 https://musewide.aip.de/project/

5 https://www.eso.org/sci/facilities/develop/instruments/muse.html

6 http://muse-vlt.eu/science/udf/

7 https://3dhst.research.yale.edu/Data.php
Table 1. Number of sources with spectroscopic redshifts from data sets used in this study, at every stage of the selection described in §2.

| Data set                          | N   | Reference |
|-----------------------------------|-----|-----------|
| Lyman-break (LBG) selected        | 90  | (1, 2)    |
| VANDELS DR4                       | 20  | (3, 4)    |
| VIMOS10                           | 43  | (5)       |
| Blind selected                    | 44  | (6)       |
| MUSE-WIDE                         | 42  | (7)       |
| MUSE HUDF                         | 9   | (8)       |
| Total                             | 248 |           |
| Total unique                      | 219 |           |
| Possible contaminants             | 34  |           |
| Possible AGN                      | 2   |           |
| Final sample                      | 183 |           |
| Total LBG selected                | 111 |           |
| Total blind selected              | 72  |           |

References: (1) McLure et al. (2018); (2) Pentericci et al. (2018); (3) Le Fèvre et al. (2015); (4) Tasca et al. (2017); (5) Balestra et al. (2010) (6) Urrutia et al. (2019); (7) Inami et al. (2017); (8) Momcheva et al. (2016).

2.2.7 Source duplication and final sample

In total we shortlist 248 sources across the above-mentioned surveys for this study, targeting galaxies based on photometric redshifts of Lyman-break selection, which we refer to as the Lyman break or LBG-selected, and those that were ‘blindly’ detected without any photometric pre-selection, which we refer to as the ‘blind selected’ sample. We note here again that although the spectroscopic surveys have different target selection strategies, we eventually require a detection in the PSF-homogenised CANDELS master photometric catalogue in GOODS-S for every source going forward.

Due to overlapping areas covered by the various spectroscopic surveys, a low fraction sources have been observed by multiple surveys. In such cases we give the highest precedence to the redshift obtained by VANDELS. In cases where the multiply detected source was not part of VANDELS, we give preference to the redshift recorded by the survey that is most sensitive out of the overlapping surveys.

Removing duplicate observations, 219 unique sources remain in our final sample and we show the breakdown of sources from various spectroscopic surveys in Table 1. We now turn our attention to filtering out sources that may suffer contamination to their LyC flux by emission from foreground sources along the line-of-sight using high-resolution HST photometry, as well as identifying possible AGN in the sample using deep X-ray data.

2.3 Identifying possible foreground contaminants

One of the biggest sources of error in the measurement of LyC signal from intermediate redshift galaxies is contamination within the aperture from emission from foreground galaxies along the line-of-sight to the source of interest (e.g. Vanzella et al. 2010). Therefore, before proceeding to measure LyC fluxes it is important to identify and remove sources that suffer from possible contamination to their LyC signal in the form of image artefacts, bright neighbouring sources or low-redshift interlopers along the line-of-sight. We adopt a series of steps, similar to Guaita et al. (2016), to filter the sample in order to maximise the accuracy of the LyC signal measurement.

Since all sources in our sample lie within the footprint of the GOODS-S field, they benefit from deep HST photometry at optical and near-infrared wavelengths from the HST Treasury Program (Dickinson et al. 2003) and through CANDELS (Grogin et al. 2011; Koekemoer et al. 2011), offering unparalleled resolution. This resolution is critical in the identification of possible foreground neighbouring sources in the vicinity of the galaxies with spectroscopic redshifts (e.g. Mostardi et al. 2015) that may strongly contaminate any LyC signal observed from the relatively lower resolution ground-based images.

To identify potential contamination, we create $20'' \times 20''$ postage stamps from images in the F435W, F606W, F775W and F850LP HST filters using publicly available images. We also create postage stamps of the same dimensions in the LyC images. Sources that appear to be isolated in the HST images, without any other component or a nearby source within $1''$ of their centroid coordinates are shortlisted for LyC signal measurement without any further filtration. An example of such a source (with postage stamp sizes of $5'' \times 5''$ for clarity) is shown in the top panel of Figure 2.

For sources that have one or more components within a radius of $1''$ of the centroid in the HST images, we must determine whether these are a part of the galaxy in question (which may have a ‘clumpy’ morphology) or whether they are possibly foreground objects (e.g. Grazian et al. 2016). In the bottom panel of Figure 2 we show an example (with $5'' \times 5''$ postage stamps for clarity) where the spectroscopically confirmed source is surrounded by a nearby source that lies within $1''$. Following Guaita et al. (2016), we examine the colours of the central galaxy and the surrounding components to identify contaminants in the following way. Using the F435W ($B$), F606W ($V$), F775W ($i$) and F850LP ($z$) images, we generate BGR colour images using the make_lupton_rgb function of astropy.visualization in $B_V$, $B_z$, $B/I_z$ and $V/I_z$. Additionally, we also produce a $V - i$ image for all sources. By then comparing the colours of the spectroscopically confirmed target and its companion(s) within $1''$, we determine whether the component(s) close to the centroid of the source is (are) part of the system or not. For example, Figure 3 shows the $V/I_z$ colour image for the source shown in the bottom panel of Figure 2, which is indicative that the companion source is likely to be a foreground contaminant.

Guaita et al. (2016) showed that the above-mentioned simpler and more computationally efficient colour-based foreground identification method is highly effective at identifying interlopers. Such an analysis also returns a comparable contamination identification fraction compared to a full SED-fitting based analysis of the individual components surrounding the spectroscopically confirmed source. We also stress that removing sources that show clumps of different colours is a highly conservative approach, as it might result in the removal of galaxies with clumpy morphologies where the individual clumps may harbour slightly different stellar populations.

Through this process, we remove 34 sources from our initial sample of 220 unique sources, representing $\approx 15\%$ of the sample and bringing the sample size of unique sources that are unlikely to suffer from foreground contamination to 186. The fraction of sources removed due to possible contamination by foreground objects is highly consistent with an expected fraction of 12.6% for $z \geq 3$ galaxies determined by Vanzella et al. (2010), down to the photometric depths considered in this study assuming a $1''$ radius for contaminant identification.

\[ \text{https://archive.stsci.edu/pub/hlsp/goods/v2/h_goods_v2.0_rdms.html} \]
A. Saxena et al.

2.4 Removing possible AGN

Finally, we remove potential AGN from our sample by cross-matching the coordinates of our sources with the *Chandra* 7 Ms source catalogue compiled by Luo et al. (2017) using a matching radius of 1.0″. The sources detected in the Luo et al. (2017) catalogue at $z \gtrsim 3$ are very likely to be AGN, owing to X-ray luminosities of $>10^{42} \text{ erg s}^{-1}$ at these redshifts (e.g. Magliocchetti et al. 2020; Saxena et al. 2020a, 2021). We identify and remove two sources with counterparts in the X-ray catalogue that are also classified as AGN in the catalogue and therefore, the total number of sources in our final sample comes to 183.

3 SED FITTING AND PHYSICAL PROPERTIES

Since the main aim of this study is to explore the dependence of LyC $f_{\text{esc}}$ on key galaxy properties such as stellar masses, star-formation rates, etc. in addition to statistically exploring the correlations between $f_{\text{esc}}$ and the strength of rest-frame nebular emission lines tracing intense star-formation such as [O ii] + H$\beta$, obtaining robust and reliable spectral energy distribution (SED) fits using high quality photometry of galaxies in our sample is crucial.

These key galaxy properties are potentially important factors that govern $f_{\text{esc}}$ from reionisation era galaxies, and in this section we use deep *HST* and *Spitzer/IRAC* photometry in the observed frame optical and near infrared bands, complemented by deep ground based $K$ band photometry in combination with reliable spectroscopic redshifts to accurately constrain the stellar population properties and dust extinction for the 183 sources in our final sample. We additionally compare the derived physical properties of galaxies in our...
sample that were LBG selected, and those that were blind selected, exploring any inherent differences in galaxies that these two selection techniques may introduce, thereby impacting the inferred $f_{\text{esc}}$.

3.1 SED derived physical properties

To determine both the properties of stellar populations as well as the [O iii] + H$\beta$ line strengths using $K$ band photometry, we simultaneously fit the stellar continuum and nebular line emission to the observed broadband photometry of galaxies in our sample. We note that since both stellar continuum and nebular emission are being simultaneously fitted, we include the line-contaminated $K$ band photometry in the fitting.

The SED fitting is performed using the Bayesian Analysis of Galaxies for Physical Inference and Parameter Estimation (BAGPIPES) code (Carnall et al. 2018). BAGPIPES is a Python based tool to generate complex galaxy model spectra, allowing flexible fitting to photometric data to derive key galaxy physical properties. As mentioned earlier, we use a combination of stellar continuum and nebular emission when fitting the SEDs. The stellar models are based on Bruzual & Charlot (2003), constructed using the Kroupa & Boily (2002) initial mass function (IMF). The nebular emission is computed using Cloudy grids (Ferland et al. 2013), with the only free parameter being the log of the ionisation parameter ($\log U$). When determining the strengths of the emission lines from these grids, the metallicity of the line-emitting gas is assumed to be the same as that of the stars.

We assume an exponentially declining star-formation history (τ-model), with stellar ages allowed to vary between 10 Myr and the age of the Universe at the observed redshift of the galaxy. The value of $\tau$ is allowed to vary between 100 Myr to 10 Gyr, with stellar metallicities allowed to vary in the range 0–1 Z$_{\odot}$, where Z$_{\odot}$ is the solar metallicity. The Calzetti et al. (2000) dust attenuation law is applied and the dust extinction, $A_{V,1600}$ is allowed to vary between 0 and 2 mag. We use flat posterior distributions for each of the parameters, which is the default choice in BAGPIPES. The nebular emission line strengths are set by the $\log U$ parameter, which we allow to vary from $-3$ to $-2$, which are the typically inferred values for $z \geq 3$ star-forming galaxies (see Nakajima et al. 2018; Saxena et al. 2020b, for example).

The chi-squared values of the best-fitting SEDs are evaluated, and individual SEDs are then visually inspected to ensure that the broad-band photometry, and crucially the $K$ band flux, are well reproduced by the best-fitting model. The best-fitting SEDs are then used to infer key physical properties for each galaxy, such as stellar age, dust attenuation, stellar mass, metallicity, star-formation rates, etc., in addition to the fluxes and rest-frame equivalent widths of the [O iii] $\lambda$5007 and the H$\beta$ lines derived from the nebular component of the best-fitting SED. Thanks to the Bayesian inference methodology of BAGPIPES, posterior distributions for all physical parameters are derived, leading to accurate uncertainty estimates.

The strength of the nebular emission that is added to the stellar continuum using BAGPIPES crucially depends on the best-fitting metallicity as well as the ionisation parameter (see Carnall et al. 2018). Although the ionisation parameter is a variable that can be controlled, the best-fitting metallicities are inferred from the broad-band SED fitting using both stellar and nebular components.

The median stellar mass (with 1σ standard deviation) derived from SED fitting of all 183 galaxies is log(M$_*/M_{\odot}$) = 9.2 ± 0.5, the median star-formation rate is $8 \pm 24$ M$_{\odot}$ yr$^{-1}$, the median stellar age is 1.5 ± 1.4 Gyr, and the median stellar metallicity is 0.6 ± 0.3 Z$_{\odot}$, where Z$_{\odot}$ is the solar metallicity (Asplund et al. 2009). Overall, the population of galaxies considered in this study are consistent with low-mass, star-formation objects with young stellar ages and low stellar metallicities.

In Figure 4 we show the distribution of the derived stellar masses and star-formation rates of all the galaxies in the final sample. We mark the LBG-selected galaxies in our sample using blue points, and the emission line selected galaxies using orange squares. The histograms of both stellar masses and SFRs for the LBG and blind selected samples are also shown. We show the star-forming main sequence at $3 < z < 4$ determined by Santini et al. (2017) using dashed lines.

The majority of galaxies in our sample lie on or around the main sequence, and that the stellar masses and star-formation rates vary over a large range. We also find that as expected, the blind selected galaxies tend to occupy the lower stellar mass end of the main-sequence, consequently also exhibiting lower star-formation rates compared to LBG-selected galaxies.

We note here, however, that owing to the magnitude limited nature of our galaxy sample, a larger fraction of galaxies with lower stellar masses detected in the spectroscopic surveys will cluster towards higher SFRs, as is evident from Figure 4, thereby resulting in an overall higher sSFR probed at lower stellar masses. Such an effect can potentially bias any possible dependence of LyC $f_{\text{esc}}$ on key galaxy properties such as stellar mass and/or sSFR.

3.2 [O iii] + H$\beta$ line strengths

The best-fitting SED includes a stellar continuum and a nebular emission line component, from which the equivalent width of the emission lines can be calculated. Particularly for the [O iii] and H$\beta$ lines that fall in the observed $K$ band broad, we measure a median EW$_0([\text{O iii}]+H\beta)$ of $\approx 230$ Å with standard deviation 225 Å, with the LBG selected sample having a median EW$_0([\text{O iii}]+H\beta)$ $\approx 236.2$ Å and the blind selected sample having a slightly lower median EW$_0([\text{O iii}]+H\beta)$ $\approx 207.2$ Å. The distribution of EW$_0([\text{O iii}]+H\beta)$ measured for LBGs and blind selected galaxies is shown in Figure 5.

The most immediate comparison for our [O iii] + H$\beta$ equivalent widths can be made with the study of Forrest et al. (2017), where using $K$ band photometry for galaxies at 2.95 $< z < 3.65$ they report an average EW$_0([\text{O iii}]+H\beta)$ $\approx 230 \pm 90$ Å, which is highly comparable to the median value we find for our sample. In Figure 6 we compare our SED derived line measurements with the best-fitting relations derived between spectroscopic measurements of the [O iii] $\lambda$5007 line and the stellar masses of a large sample of star-forming galaxies at $z \approx 2$ as part of the MOSDEF survey (Reddy et al. 2018).

We additionally show the stellar mass dependence of the [O iii] line derived for a sample of extreme emission line galaxies (defined as EW$_0([\text{O iii}]) > 225$ Å by Tang et al. 2019) at $z \approx 2$ by Tang et al. (2019), which also exhibit lower stellar masses. We find that the distribution of EW$_0([\text{O iii}])$ as a function of stellar mass for galaxies in our sample broadly agrees with the best-fitting relation derived from MOSDEF at higher stellar masses. The scatter around the best-fitting relation observed in our sample is also consistent with what was reported by Reddy et al. (2018).

We identify 59 galaxies in our sample that can be classified as extreme emission line galaxies (EELGs), with EW$_0([\text{O iii}]+H\beta) > 300$ Å (e.g. Stark 2016)). The median EW$_0([\text{O iii}]+H\beta)$ in the EELG sample is $\approx 500$ Å, which is slightly lower than the range of $\approx 660 - 800$ Å reported by Forrest et al. (2017) for EELGs in their sample.

To further investigate the reliability of our inferred [O iii] + H$\beta$ line strengths, we compare our rest-frame [O iii] + H$\beta$ equivalent

---

**LyC leakage at z ~ 3 – 3.5**

---

**MNRAAS 000, 1–18 (2021)**
Figure 4. Distribution of SED derived stellar masses and star-formation rates for galaxies in the final sample, colour coded by metallicity. The dashed line shows the star-forming main sequence derived by Santini et al. (2017) at redshifts $3 < z < 4$. We find that most of our galaxies lie on the main sequence, and span a range of masses and star-formation rates, which makes them representative of the general galaxy population at $z \sim 3.3$.

Figure 5. Histogram of the rest-frame $[O\text{iii}] + H\beta$ equivalent widths measured for LBG-selected galaxies (blue) and blind selected galaxies (orange) in our sample using SED fitting. The median $\text{EW}_0([O\text{iii}] + H\beta)$ of the full sample is 228.6 Å, and the derived equivalent widths follow a log-normal distribution (similar to that reported by Stark et al. 2013). The EW distributions for both LBGs and emission line galaxies are comparable, with the median values (dashed lines and text) highly consistent with each other.

width measurements as a function of galaxy stellar to results from the MOSDEF spectroscopic survey (Kriek et al. 2015), which spectroscopically observed a sample of $\sim 1200$ star-forming galaxies at redshifts $1.4 \leq z \leq 3.8$ (Reddy et al. 2018) in Figure 6. We find that our measurements at $z \sim 3 - 3.5$ broadly agree with the best-fitting relation obtained by Reddy et al. (2018), with comparable scatter at stellar masses $> 10^9 M_\odot$.

We also compare EWs of galaxies in our sample that may be considered as EELGs following the Tang et al. (2019) classification ($\text{EW}_0([O\text{iii}]) > 225\text{Å}$) with spectroscopic measurements at $z \sim 2$ from Tang et al. (2019), finding broad agreement with their best-fitting relation (Tang et al., private communication), which is also shown in Figure 6.

Our EELG $[O\text{iii}] + H\beta$ EWs are also comparable with photometrically selected extreme line emitters found at $z > 6$ – Endsley et al. (2020) measured a median value of $\text{EW}_0([O\text{iii}] + H\beta) \sim 700 \text{Å}$ for star-forming galaxies at $z \sim 7$ and Labbé et al. (2013) found an average rest frame $[O\text{iii}] + H\beta$ EW of 670 ± 200 Å at $z \sim 8$. Additionally, Smit et al. (2015) identified galaxies with extreme Spitzer/IRAC colours at $z \sim 6.8$ and found that 50% of the strongest line emitters have $\text{EW}_0([O\text{iii}] + H\beta) \sim 1085 \text{Å}$. Using a similar technique, Roberts-Borsani et al. (2016) identified four bright galaxies at $z \sim 7$ with $\text{EW}_0([O\text{iii}] + H\beta) \sim 1500 \text{Å}$, all of which have been confirmed to be strong Ly$\alpha$ emitters. Further, Castellano et al. (2017) measured an average $\text{EW}([O\text{iii}] + H\beta)$ of $\sim 1500 \text{Å}$ for Ly$\alpha$ emitting galaxies at $z \sim 6.8$. Therefore, our sample of EELGs at $z \sim 3 - 3.5$ offers an
excellent opportunity to study the escaping ionising radiation from analogues of reionisation-era galaxies.

We note here, however, that the line strengths of some of the brightest $[\text{O} \text{ III}]$ emitting galaxies, particularly those with fainter continua, may be underestimated due to the lower limit on the ionisation parameter of $\sim -2.0$ permitted by BAGPIPES as well as the depth of photometric data in the $K$ band. We further note that the flux (and consequently stellar mass) limited nature of our galaxy sample naturally results in incompleteness of EELGs down to lower stellar masses.

3.3 Comparison with NIR spectroscopic observations

To test the accuracy of the inferred $[\text{O} \text{ III}] + \text{H} \beta$ strengths from SED fitting, we compare our measurements with near-IR observations of a subset of VANDELS galaxies in the CDFS and UDS fields in the redshift range $z \sim 3 - 4$ using MOSFIRE on Keck Telescope, as part of the recently completed NIRVANDELS survey (Cullen et al. 2021). We note that only a fraction of NIRVANDELS galaxies in the CDFS field are also part of the final sample in this study.

To do this, we fit SEDs to all NIRVANDELS galaxies using the same SED fitting parameters and techniques that we used for the main galaxy sample described in §3 and compare the observed and SED-derived $[\text{O} \text{ III}]$ line fluxes. The comparison between the SED derived and observed $[\text{O} \text{ III}]$ line fluxes for NIRVANDELS galaxies is shown in Figure 7, with the dashed line marking the one-to-one relation. The error bars shown on the SED derived line fluxes are at the 20% level. We find that the SED derived line fluxes are remarkably close to the observed values (within $\sim 0.3$ dex) over a broad flux range. We therefore conclude that simultaneously fitting the stellar continuum and nebular line emission with the ionisation parameter in the range $-3 \leq \log U \leq -2$ gives realistic estimates of the $[\text{O} \text{ III}]$ (and $\text{H} \beta$) line fluxes for galaxies in our sample.

Having fitted SEDs to all 183 unique galaxies in our final sample and measured key galaxy properties as well as $[\text{O} \text{ III}]$ and $\text{H} \beta$ line strengths, we now proceed to measure LyC fluxes for galaxies using the available LyC images.

4 Lyman continuum escape fraction

4.1 Measuring $f_{\text{esc}}$ and $f_{\text{rel}}$

In this section, we describe our methodology for measuring the LyC flux from the available LyC images. Since these filters cover slightly different rest-frame LyC wavelengths at different redshifts as mentioned in §2.1, we split our sample into the relevant redshift bins corresponding to LyC coverage offered by the filters. $\text{NB3727}$ includes 79 galaxies, $\text{NB396}$ includes 83 galaxies, and $U$ includes 91 galaxies. We show the number of galaxies and the redshift ranges corresponding to each LyC filter along with $1\sigma$ depths in Table 2.

We note that owing to the overlapping wavelength coverage offered by the the $\text{NB396}$ and the $U$-band filter, some galaxies are included in both subsets.

An important parameter quantifying the escape of LyC photons from a galaxy in a dust-independent manner is the relative $f_{\text{esc}}$, or $f_{\text{esc}}$ (Steidel et al. 2001), comparing the observed ratio of ionising to non-ionising UV flux to the intrinsically produced ratio by stellar populations within the galaxy, corrected for absorption by the intervening neutral IGM. If the intrinsic ratio of luminosities at $\sim 1400 \, \AA$ and $\sim 900 \, \AA$, $(L_{1400}/L_{900})_{\text{int}}$ is known (e.g. from stellar population modelling), then $f_{\text{esc}}$ can be calculated as

$$f_{\text{esc}} = \left( \frac{F_{900}}{F_{1400}} \right)_{\text{obs}} \times \left( \frac{L_{1400}}{L_{900}} \right)_{\text{int}} \times \frac{1}{\tau_{900}} \times \exp \left( -\tau_{900} \right) \tag{1}$$

where $(F_{900}/F_{1400})_{\text{obs}}$ is the observed ratio of the ionising LyC flux to non-ionising UV flux at $\sim 1400 \, \AA$, and $\tau_{900}$ is the transmissivity of ionising photons (at 900 Å) through the intervening IGM (Siana et al. 2007). The absolute escape fraction, $f_{\text{esc}}$, can then be calculated...
from $f_{\text{esc}}$ by applying a dust correction as follows

$$f_{\text{esc}} = f_{\text{esc}}^\text{rel} \times 10^{(-0.4 \times A_{1400})}$$

(2)

where $A_{1400} = 10.33 \times E(B-V)$ according to the Calzetti et al. (2000) dust reddening law. Therefore, to calculate $f_{\text{esc}}$ we must constrain each of these ingredients in equations (1) and (2), and below we highlight how these are calculated for our galaxies.

### 4.1.1 LyC flux measurement

The observed flux ratios in the equations above require a measurement of the LyC flux, which we measure from the available LyC images using aperture photometry. Photometry in the LyC images is performed by placing circular apertures at the coordinates in the CANDELS catalogues using the PYTHON package photutils (Bradley et al. 2020). The average PSF of the NB3727 image is 1.4$''$, of the NB396 is 0.94$''$ (Guaita et al. 2016) and of the U image is 0.8$''$ (Nonino et al. 2009). The radius of the circular aperture is set to either match or be slightly larger than the PSF to capture small-scale PSF variations across the LyC images. Therefore, we use an aperture with radius 0.7$''$ for NB3727 and 0.5$''$ for NB396 and U band images.

We measure the local background noise around the apertures by placing a circular annulus (at the same positions as the aperture) with an inner radius of 2$''$ and an outer radius of 3$''$. For galaxies in which the flux measured in the aperture was lower than the background flux measured in the annulus, we assigned a limiting LyC flux value equal to the local background noise with a 100% error.

The non-ionising UV flux is calculated from the F606W HST image, which covers the rest-frame ~ 1400 Å wavelengths for the redshift range of galaxies in this study. Therefore, the ratio of the flux determined from the LyC bands and from the F606W band gives us a measure of the term $(F_{900}/F_{1400})_{\text{obs}}$.

### 4.1.2 Intrinsic non-ionising to ionising luminosity ratio

The intrinsic ratio between UV luminosity at non-ionising wavelengths (e.g. ~ 1400 Å) and LyC wavelengths (~ 900 Å) is calculated individually for each source using the best-fitting SED. We create synthetic SEDs using the best-fitting stellar population parameters determined and measure the intrinsic ratios, $L_{1400}/L_{900}$, for each galaxy.

We find an average intrinsic ratio of 4.5, with a standard deviation of 0.7. Individual intrinsic ratio measurements for each galaxy enabled by accurate spectroscopic redshifts lead to a more accurate $f_{\text{esc}}$ calculation for individual galaxies compared assuming an average intrinsic ratio for all galaxies in the sample, as done by previous studies measuring LyC $f_{\text{esc}}$ at $z \sim 3$, where the assumed intrinsic ratio took values of 3 (Steidel et al. 2001; Grazian et al. 2016, 2017; Marchi et al. 2017b), 5 (Guaita et al. 2016; Vanzella et al. 2016a) or 7 (Fletcher et al. 2019).

### 4.1.3 IGM transmissivity

We calculate the IGM transmissivity of LyC photons for each galaxy using the prescriptions of Steidel et al. (2018). In addition to the IGM transmission, the Steidel et al. (2018) model also takes into account the effects of transmission through the circum-galactic medium (CGM) surrounding each galaxy in the so-called “IGM+CGM” model. This results in an average LyC transmission, $\exp(-\tau_{900}) = 0.371$ at $z = 3.0$ and a much lower $\exp(-\tau_{900}) = 0.264$ at $z = 3.5$.

An advantage of having spectroscopic redshifts is that the IGM transmissivity can be accurately calculated for each source at the rest-frame wavelength of 900 Å, the $\tau_{900}$. Hence, we calculate the LyC transmission through both the IGM and the CGM, or $\exp(-\tau_{900})$ for each galaxy in our final sample.

### 4.1.4 Dust attenuation

Finally, the dust attenuation (or $A_{1400}$) for each source is calculated from the best-fitting SED. During the SED fitting process we allowed $A_{1400}$ to vary between 0 and 2, which naturally limits the derived values. This means that our SED fits will miss any significantly dusty galaxies, but given the high-redshift star-forming nature of these galaxies, heavy dust obscuration is unlikely to be the case. We find an average dust attenuation of $A_{1400} = 0.40$ mag in our sample with a standard deviation of 0.26 mag.

Having defined the necessary ingredients to calculate $f_{\text{esc}}$ for each source and described the measurements of each of these parameters, in the following section we present the our measurements of the relative and the absolute escape fractions of LyC photons from each galaxy.

### 4.2 Individual LyC $f_{\text{esc}}$ measurements

We measure non-zero LyC $f_{\text{esc}}$ at $\gtrsim 2\sigma$ significance levels in 11 out of 183 galaxies in our sample. The LyC $f_{\text{esc}}$ is in the range of 0.14 – 0.85, and the galaxies showing non-zero $f_{\text{esc}}$ span a wide range of stellar masses ($M_\star = 10^{8.3} – 10^{9.7} M_\odot$), star-formation rates (SFR = 2.3 – 37.4 $M_\odot$ yr$^{-1}$) and [O iii] + Hβ equivalent widths (EW$_{\lambda}$[O iii] + Hβ) = 111.8 – 1160.3 Å).

We note that 8 out of 11 candidate LyC leakers were LBG selected, and 3 were blindly selected for spectroscopic follow-up. The galaxy with the highest measured $f_{\text{esc}} = 0.85 \pm 0.33$ (CDFS 13385) was blindly selected from the MUSE-HUDF survey and has a relatively low stellar mass of $10^{8.3} M_\odot$, showing extreme [O iii] + Hβ line emission through its K band photometry.

The best-fitting SED derived physical parameters for these 11 candidate LyC leaking galaxies are given in Table 3, and the measured quantities (both through SED fitting and aperture photometry) used to calculate $f_{\text{esc}}^\text{rel}$ and $f_{\text{esc}}$ are given in Table 4. The 5$'' \times 5''$ cutout galleries showing the LyC image and the observed-frame optical HST photometry, along with the best-fitting SEDs for the 11 LyC leaker candidates are shown in Appendix A. A full spectroscopic analysis of these 11 LyC leaking candidates is beyond the scope of this paper.
the present paper and will be explored in greater detail in forthcoming publications.

It is important to note that given the stochasticity of the IGM attenuation at these redshifts (see for example Bassett et al. 2021), it is hard to accurately determine the absolute LyC $f_{\text{esc}}$ for sources at $z \geq 3$. Therefore, the IGM stochasticity introduces an unavoidable element of scatter in the $f_{\text{esc}}$ measurements, which in turn may be an important source of scatter in the correlations between $f_{\text{esc}}$ and key galaxy properties that will be investigated in the sections that follow. We will discuss the effects of IGM stochasticity on the inferred LyC $f_{\text{esc}}$ measurements in §6.

Given the relatively large sample size of 183 sources, we expect $\sim 4$ sources to appear as noise fluctuations at the $2\sigma$ level. From Table 4 we note that 4 out of 11 sources identified as candidate LyC leakers are close to the $2\sigma$ confidence level in their respective LyC images and could be consistent with noise fluctuations. Deeper photometric data at LyC wavelengths is needed to confirm the LyC leaking nature of these sources.

Apart from the 11 candidate LyC leakers, all galaxies in our sample remain undetected at $\geq 2\sigma$ levels in the available LyC images, indicating that the global $f_{\text{esc}}$ from star-forming galaxies at $z = 3–3.5$ must be low. In the sections that follow we derive the global $f_{\text{esc}}$ from different populations of galaxies in our sample through stacking the low-significance LyC fluxes measured from the majority of galaxies, and use these stacked measurements to set additional constraints on any global dependence of $f_{\text{esc}}$ on key galaxy properties traced by sub-populations of galaxies within our sample.

4.3 Stacked LyC $f_{\text{esc}}$ measurements

Only $\sim 6\%$ galaxies in our sample have a $\geq 2\sigma$ detection in the LyC images. Therefore, to constrain the global $f_{\text{esc}}$ we must co-add the LyC signal from galaxies that were not classified as candidate LyC leakers. To do this, we first remove the 11 individual LyC leakers from the stacking sample and employ both the stacking of LyC images, as well as co-adding the LyC flux measured through aperture photometry as described below.

We first investigate whether any LyC signal can be measured through stacking the LyC images of individual galaxies falling within the redshift coverage of each LyC filter. To do this, we produce $10^5 \times 10^6$ cutouts of both the LyC image and the corresponding root-mean-squared (RMS) error image centred on the CANDELS coordinates for galaxies that are not individual LyC leakers. We then apply $5\sigma$ clipping to the cutouts to masks bright pixels that could bias the stacked image. We then co-add the sigma-clipped cutouts using a weighted averaging method, where the corresponding RMS of each pixel of the galaxy cutout is used to assign a weight to the pixels of each galaxy cutout. In Figure 8 we show the results from stacking the LyC cutouts for each of the filters and as can be seen, we do not find any statistically significant LyC signal even in the stacked NB3727, NB396 and $U$ band images, consistent with that reported by Guaita et al. (2016) from the two narrow bands and by Naidu et al. (2018) from the $U$ broad band.

Instead of extracting a flux from these stacked LyC images and relying on the sample averaged values for the intrinsic non-ionising to ionising UV ratio, IGM transmissivity and dust attenuation to calculate $f_{\text{esc}}$, we use a slightly different approach and derive global $f_{\text{esc}}$ using the standard deviation of the weighted average of the individual LyC fluxes measured through aperture photometry across the available LyC images as described in §4.1.1 (see also Guaita et al. 2016). The weight assigned to the $f_{\text{esc}}$ measurement for each source is the inverse square of the error on $f_{\text{esc}}$, or $1/\Delta f_{\text{esc}}^2$.

4.3.1 LyC $f_{\text{esc}}$ from LBG and blind selected galaxies

Out of the 172 galaxies that were not identified as individual LyC detections, 103 are LBG selected and 69 are blindly selected. Using weighted averaging, we derive $1\sigma$ $f_{\text{esc}}$ limits of $< 0.11$ for the LBG selected and a slightly higher $1\sigma$ limit of $< 0.13$ for the blind selected sample. We note here that since the blind selected sample is also fainter in UV magnitudes, the flux limited nature of the available LyC images may bias the inferred $f_{\text{esc}}$ to higher values.

A LyC $f_{\text{esc}} < 0.11$ for our LBG selected sample is comparable with $f_{\text{esc}} \approx 0.09$ reported by Steidel et al. (2018) by stacking deep UV spectra of $z \sim 3$ LBGs and $f_{\text{esc}} \approx 0.06$ obtained by a later reanalysis of the Steidel et al. (2018) sample by Pahl et al. (2021), and with other measurements from LBGs at $z \sim 3$ (e.g. Grazian et al. 2016; Guaita et al. 2016; Marchi et al. 2017a; Naidu et al. 2018; Meštric et al. 2021). The slightly higher $1\sigma$ $f_{\text{esc}}$ limit of $f_{\text{esc}} < 0.13$ measured for blind-selected galaxies is also consistent with measurements of emission-line selected galaxies at $z = 2–4$ (e.g. Mostardi et al. 2015; Japelj et al. 2017; Ji et al. 2020; Smith et al. 2020).

Figure 8. Stacked image from all sources in NB3727 (left), NB396 (middle) and $U$ band (right). We do not see any statistically significant flux in any of the stacked images.

After background subtraction, the weighted average of sources that are not classified as candidate LyC leakers would be expected to be close to zero, with the standard deviation providing a robust $1\sigma$ upper limit on the LyC signal from the sample (see also Guaita et al. 2016). This method takes full advantage of the availability of spectroscopic redshifts and accurate SED fitting that enable reliable measurements of both the values, errors and limits on individual $f_{\text{esc}}$ and $f_{\text{esc}}$ for each galaxy.

Galaxies in the redshift range covered by NB3727 do not overlap with the other two LyC filters. However, galaxies with redshift between 3.41–3.49 have overlapping LyC coverage in both NB396 and $U$ images. Therefore, to assign a LyC flux $f_{\text{esc}}$ and $f_{\text{esc}}$ to each unique galaxy in our sample, we prioritise the flux measured from the LyC image with a lower error, which translates to a lower error on $f_{\text{esc}}$. We note here that $f_{\text{esc}}$ measurements/limits recorded using both LyC filters are broadly in agreement with each other.

Using the standard deviation of the weighted average of LyC flux from the unique sample of galaxies that are not individually identified as LyC leakers, we obtain a $1\sigma$ upper limit of $f_{\text{esc}} < 0.12$. We additionally calculate the stacked $f_{\text{esc}}$ limit obtained from all galaxies in the sample (i.e. both LyC detections and non-detections) finding a slightly higher $1\sigma$ limit of $f_{\text{esc}} < 0.16$, which is not surprising. This stacked measurement from the full sample potentially helps minimise the effects of stochastic IGM transmission along the line of sight, which we discuss further in §6.
Table 3. Nature of selection for each galaxy, with LBG representing Lyman-break selected and BLD representing blind selection, as well as best-fitting SED derived physical properties for candidate LyC leaking galaxies. Also given is the LyC detection filter for each source.

| CANDELS ID | Sample | Survey | z   | LyC filter | log(M_*/M_☉) | SFR (M_☉ yr⁻¹) | log(sSFR yr⁻¹) | EW_0 ([O iii] + Hβ) (Å) |
|------------|--------|--------|-----|------------|--------------|----------------|----------------|------------------------|
| CDFS 5161  | LBG    | VANDELS| 3.40| NB396      | 9.3          | 16.3           | -8.1           | 268.2                  |
| CDFS 9358  | LBG    | VIMOS10| 3.29| NB3727     | 9.6          | 37.0           | -8.1           | 231.3                  |
| CDFS 9692  | LBG    | VANDELS| 3.40| NB396      | 9.3          | 2.3            | -8.0           | 1160.3                 |
| CDFS 12448 | LBG    | VANDELS| 3.40| U          | 9.6          | 12.5           | -8.5           | 119.3                  |
| CDFS 13385 | BLD    | MUSE HUDF| 3.43| U          | 8.6          | 3.6            | -8.1           | 334.6                  |
| CDFS 15718 | BLD    | MUSE HUDF| 3.43| NB396      | 8.3          | 2.0            | -8.0           | 986.8                  |
| CDFS 16444 | BLD    | MUSE HUDF| 3.12| NB3727     | 9.3          | 23.1           | -7.9           | 456.4                  |
| CDFS 18454 | BLD    | MUSE HUDF| 3.16| NB3727     | 9.2          | 16.7           | -8.0           | 339.8                  |
| CDFS 19872 | LBG    | VANDELS| 3.42| NB396      | 9.6          | 5.6            | -8.8           | 111.8                  |
| CDFS 20745 | LBG    | VANDELS| 3.41| NB396      | 9.0          | 5.5            | -8.3           | 400.6                  |
| CDFS 24975 | LBG    | VANDELS| 3.18| NB3727     | 9.7          | 19.8           | -8.5           | 214.9                  |

Table 4. Parameters required for the calculation of fesc_H and fesc for candidate LyC leakers identified in this study.

| CANDELS ID | z | (L_1400/L_900)_int | A_V (mag) | F_900 (µJy) | (F_900/F_1400)_obs | <exp(-τ_900)> | f_esc_H | f_esc |
|------------|---|-------------------|----------|------------|-------------------|---------------|--------|-------|
| CDFS 5161  | 3.40| 0.6 ± 0.1         | 0.036 ± 0.015 | 0.07 ± 0.02 | 0.28               | 0.91 ± 0.39   | 0.53 ± 0.24 |
| CDFS 9358  | 3.29| 3.4               | 0.048 ± 0.020 | 0.02 ± 0.01 | 0.32               | 0.21 ± 0.11   | 0.14 ± 0.07 |
| CDFS 9692  | 3.47| 2.3               | 0.039 ± 0.020 | 0.06 ± 0.03 | 0.27               | 0.55 ± 0.25   | 0.38 ± 0.19 |
| CDFS 12448 | 3.46| 4.1               | 0.006 ± 0.001 | 0.02 ± 0.01 | 0.27               | 0.24 ± 0.10   | 0.20 ± 0.12 |
| CDFS 13385 | 3.43| 3.5               | 0.009 ± 0.002 | 0.09 ± 0.02 | 0.28               | 1.12 ± 0.24   | 0.85 ± 0.33 |
| CDFS 15718 | 3.43| 2.0               | 0.034 ± 0.009 | 0.06 ± 0.02 | 0.28               | 0.42 ± 0.12   | 0.28 ± 0.10 |
| CDFS 16444 | 3.12| 3.0               | 0.068 ± 0.014 | 0.06 ± 0.01 | 0.34               | 0.55 ± 0.11   | 0.30 ± 0.07 |
| CDFS 18454 | 3.16| 2.2               | 0.045 ± 0.021 | 0.04 ± 0.02 | 0.34               | 0.42 ± 0.21   | 0.20 ± 0.10 |
| CDFS 19872 | 3.45| 4.0               | 0.01 ± 0.01   | 0.040 ± 0.020 | 0.02 ± 0.01 | 0.28       | 0.32 ± 0.16 | 0.29 ± 0.30 |
| CDFS 20745 | 3.49| 4.0               | 0.033 ± 0.015 | 0.03 ± 0.02 | 0.27               | 0.45 ± 0.23   | 0.38 ± 0.30 |
| CDFS 24975 | 3.18| 3.4               | 0.043 ± 0.021 | 0.05 ± 0.02 | 0.33               | 0.53 ± 0.21   | 0.27 ± 0.11 |

4.3.2 LyC fesc from extreme emission line galaxies (EELGs)

In this section we investigate the stacked fesc measurements of the previously identified extreme emission line galaxies (EELGs; EW_0([O iii] + Hβ) ≥ 300 Å) as well as normal emission line galaxies (ELGs; EW_0([O iii] + Hβ) < 300 Å) in our sample (see §3.2). For this analysis we include the 11 candidate LyC leakers to better understand the dependence of fesc on [O iii] + Hβ EWs.

There are 59 EELGs and 124 ELGs in our sample. The average EW_0([O iii] + Hβ) for EELGs is 421.2 Å and the average EW_0([O iii] + Hβ) for ELGs is 183.5 Å. By once again calculating the weighted average of fesc for ELGs and EELGs, we determine 1σ upper limits of fesc < 0.14 for ELGs and fesc < 0.20 for EELGs. We note here that we obtain slightly higher fesc limits from bins created based on emission line strengths compared to the LBG and blind-selected samples because the individually identified LyC leakers are included in the ELG and EELG bins.

Qualitatively speaking, the distribution of [O iii] + Hβ EWs measured for individual LyC leakers is similar to the distribution of the parent sample, implying that the individual LyC leakers seem to have been randomly drawn from the parent sample at least in terms of [O iii] + Hβ EWs. This is consistent with what was reported by Nakajima et al. (2020) for a sample of LAEs at z ~ 3, where the [O iii] + Hβ EWs of LAEs that are LyC leakers and non-leakers are not significantly different.

In Table 5 we give the median galaxy physical properties and the measured fesc for subsets created based on the initial spectroscopic selection method, as well as on the strength of [O iii] + Hβ emission lines. No clear differences in fesc are seen between these subsets, posing questions surrounding the origin of leaking LyC radiation from only a low fraction of galaxies at intermediate redshifts. In the following section we investigate the dependence of fesc on key galaxy properties for both candidate LyC leakers and stacks of galaxies.

5 RESULTS

Having measured LyC fluxes and fesc values for every source in the sample, and having used stacking to establish fesc limits from the sample of galaxies that do not show any LyC leakage, in this section we explore potential correlations between fesc and the properties of the underlying stellar population in the galaxies. Constraining the dependence of fesc on these key galaxy properties is important to understand the key drivers of reionisation at z > 6, and here we rely on robust SED-fitting based measurements to explore these.

5.1 Dependence of fesc on stellar mass

We first explore the dependence of fesc on the stellar masses of galaxies. In Figure 9 we show the fesc measured for the candidate LyC leaking candidates as well as the stacked limits obtained for the sub samples of LBG and blind selected galaxies in our sample. As reported in §3.1, the median stellar mass of LBG selected galaxies is 10^{9.5} M_☉ and that of the blind selected galaxies is 10^{9.0} M_☉.

We find that the candidate LyC leaking galaxies occupy a large range of stellar masses, ranging from 10^{8.8} - 10^{7.7} M_☉. The galaxy with the highest fesc in our sample, CDFS 13385 at z = 3.431 with fesc = 0.85 ± 0.33 has a stellar mass of ≈ 10^{6.3} M_☉, which is lower than the stellar masses of known LyC leaking galaxies with fesc > 0.5 at z ≥ 3 such as Ion2 (de Barros et al. 2016; Vanzella et al. 2016a), Ion3 (Vanzella et al. 2018) and Q1549–C25 (Shapley et al. 2016), and comparable to the stellar masses of LyC leaking LAEs identified by Fletcher et al. (2019). The LyC leaker with the highest stellar masses in our sample has M_* ≈ 10^{9.7} – CDFS 24975 at z = 3.187 with fesc = 0.27 ± 0.11.

We use least-squares fitting to obtain the best-fitting parameters for the function fesc = A log(M_*/M_☉) + B, finding A = -0.10 ± 0.02 and B = 1.17 ± 0.40 (solid green line in Figure 9). The slope of the
Table 5. Physical properties and $f_{\text{esc}}$ for LBG or blind selected galaxies, ELGs and EELGs, and the full sample. Note that the LBG and blind selected subsets are created only for those galaxies that are undetected in the LyC images at $\geq 2\sigma$ level, but the ELG and EELG subsets include the individual LyC leakers as well.

| Subset                        | $N$  | $\log(M_*/M_\odot)$ | $\log(sSFR/\text{yr}^{-1})$ | $\text{EW}_0 ([\text{O} \text{~III}] + \text{H}\beta)$ (Å) | $f_{\text{esc}}$ |
|-------------------------------|------|----------------------|-------------------------------|----------------------------------------------------------|----------------|
| LBG selected, LyC non-detections | 103  | 9.4                  | $-8.2$                        | 236.2                                                    | $< 0.11$       |
| Blind selected, LyC non-detections | 69   | 9.0                  | $-8.3$                        | 207.2                                                    | $< 0.13$       |
| ELGs (all) $-$ EW$_0 ([\text{O} \text{~III}] + \text{H}\beta) < 300$ Å  | 124  | 9.3                  | $-8.3$                        | 183.5                                                    | $< 0.14$       |
| EELGs (all) $-$ EW$_0 ([\text{O} \text{~III}] + \text{H}\beta) \geq 300$ Å  | 59   | 8.9                  | $-8.0$                        | 421.2                                                    | $< 0.20$       |
| Full sample  | 183  | 9.2                  | $-8.3$                        | 230.9                                                    | $< 0.16$       |

Figure 9. LyC $f_{\text{esc}}$ as a function of stellar mass for candidate LyC leakers in our sample (green points), and stacked measurements from LBG selected (blue arrow), blind-selected galaxies (orange arrow) and the sample average (black arrow) in this study. The number of galaxies used in the stacking measurement are also given. We find a very week correlation between $f_{\text{esc}}$ and stellar mass, with a best-fitting slope $-0.10 \pm 0.02$ (solid green line, uncertainty in shaded region). This dependence on stellar mass is stronger that the recently observed lack of correlation between the two quantities for a sample of low mass ($< 10^{8} M_* )$ galaxies at $0.3 \leq z \leq 0.45$ by Izotov et al. (2021), however the scatter is very large. We note that the stacked limits are not included when obtaining the best-fitting relations in this study.

Figure 10. Distribution of $f_{\text{esc}}$ and sSFR of candidate LyC leakers, LBG and blind-selected galaxies as well as the sample average (same legend as Figure 9). We find little to no correlation between $f_{\text{esc}}$ and sSFR of individual LyC leakers at the $2\sigma$ confidence level, with a best-fitting slope $-0.028 \pm 0.015$ (solid green line with uncertainty in shaded region). The stacked $f_{\text{esc}}$ values derived from LBG and blind-selected samples are consistent with the best-fitting relation. The lack of dependence of $f_{\text{esc}}$ on sSFR has also been seen in simulations (e.g. Yoo et al. 2020).

5.2 Dependence of $f_{\text{esc}}$ on specific SFR

We now investigate correlations between $f_{\text{esc}}$ and specific SFR (sSFR), which is the star-formation rate per unit stellar mass of a galaxy. The distribution of $f_{\text{esc}}$ and sSFR for both the candidate LyC leakers and stacks of LBG and blind selected galaxies is shown in Figure 10. As reported in §3.1, the blind selected galaxies in our sample have a slightly lower median specific SFR of $\log(\text{sSFR/yr}^{-1}) = -8.3$ compared to $\log(\text{sSFR/yr}^{-1}) = -8.2$ for LBG selected galaxies.

The candidate LyC leakers cover a large range of sSFRs, from $\log(\text{sSFR/yr}^{-1}) \approx -8.8$ to $\log(\text{sSFR/yr}^{-1}) \approx -7.9$. We note that the majority of LyC leaking candidates (seven out of 11) have relatively high sSFR values, with $\log(\text{sSFR/yr}^{-1}) > -8.1$, comparable to LyC leaking LAEs from Fletcher et al. (2019). In particular, the strongest LyC leaker in our sample, CDFS 13385, has $\log(\text{sSFR/yr}^{-1}) = -8.1$, which is lower than Iom2 and Iom3 but more than an order of magnitude higher than Q1549–C25 (Shapley et al. 2016).

To quantify the dependence of $f_{\text{esc}}$ on sSFR, we again use least-squares fitting and obtain best-fitting correlations to the function $f_{\text{esc}} = C \log(\text{sSFR/yr}^{-1}) + D$ with a slope of $C = -0.028 \pm 0.015$ (solid green line in Figure 10). This best-fitting suggests a very weak decrease of $f_{\text{esc}}$ with increasing sSFR, but is consistent with no dependence of $f_{\text{esc}}$ on sSFR at the $\approx 2\sigma$ confidence level, consistent with what has been reported from disc galaxy simulations at high redshifts (e.g. Yoo et al. 2020).

Assuming that the stellar mass of a galaxy is closely linked to its size at UV wavelengths, no strong dependence of $f_{\text{esc}}$ on sSFR may also translate to no strong dependence of $f_{\text{esc}}$ on the star-formation surface density of galaxies (e.g. Model II of Naidu et al. 2020). This may have bearing on the dominant contribution of the UV brightest sources towards reionisation, and accurate size measurements of our candidates LyC leakers that will be explored in a future study will help robustly test the dependence of $f_{\text{esc}}$ on SFR surface densities.
5.3 Dependence of $f_{\text{esc}}$ on [O III] $\lambda 5007$ and H$\beta$

In this section we investigate the dependence of $f_{\text{esc}}$ on the [O III] $\lambda 5007$ and H$\beta$ line strengths for galaxies in our sample. In Figure 11 we show the $f_{\text{esc}}$ and the log of EW$_{\text{esc}}$([O III] $\lambda 5007$ + H$\beta$) for individual LyC leakers (green points) as well limits derived for normal emission line galaxies (ELGs; red arrow) and and extreme emission line galaxies (EELGs; brown arrow), which were defined in §4.3.2. We note that 6 out of the 11 individual LyC leakers can be classified as EELGs, with EW$_{\text{esc}}$([O III] $\lambda 5007$ + H$\beta$) $> 300$ Å.

For the individual LyC leaking candidates, CDFS 9692 at $z = 3.470$ with $f_{\text{esc}} = 0.38 \pm 0.19$ has the highest EW$_{\text{esc}}$([O III] $\lambda 5007$ + H$\beta$) value of 1160.3 Å. The strongest LyC leaker, CDFS 13385, also shows extreme [O III] $\lambda 5007$ + H$\beta$ line fluxes, with EW$_{\text{esc}}$([O III] $\lambda 5007$ + H$\beta$) = 986.8 Å, in line with expectations from galaxies with high $f_{\text{esc}}$. However, overall we do not find consistently high [O III] $\lambda 5007$ + H$\beta$ EWs across our candidate LyC leaking galaxies. Similarly, as reported in §4.3.2 we do not find a considerably higher $f_{\text{esc}}$ using stacking for EELGs compared to the sample of ELGs, but do find that the $f_{\text{esc}}$ limit for EELGs is higher than that for ELGs.

A best-fitting relation between $f_{\text{esc}}$ and [O III] $\lambda 5007$ + H$\beta$ line strengths shows a positive correlation, indicating that galaxies with higher $f_{\text{esc}}$ also tend to show stronger [O III] $\lambda 5007$ + H$\beta$ lines, shown in Figure 11. The best-fitting relation has a positive slope of 0.15 $\pm$ 0.04, indicative of a mild dependence of $f_{\text{esc}}$ on rest-frame [O III] $\lambda 5007$ + H$\beta$ EW, with the general trend of increasing $f_{\text{esc}}$ at higher [O III] $\lambda 5007$ + H$\beta$ strengths consistent with what has been seen in the local Universe (e.g. Izotov et al. 2018a). The higher $f_{\text{esc}}$ upper limit of $< 0.20$ seen for EELGs compared to $f_{\text{esc}} < 0.14$ seen for ELGs is also consistent with the best-fitting relation obtained.

NIR spectroscopy of LyC leaking LAEs from the Fletcher et al. (2019) sample presented by Nakajima et al. (2020), however, did not find uniformly high [O III] $\lambda 5007$ + H$\beta$ line strengths for LyC leakers, which is consistent with our findings. Izotov et al. (2018a) reported a large spread in the $f_{\text{esc}}$ values of local LyC leaking galaxies with high [O III] $\lambda 5007$ line strengths. Therefore, there is increasing evidence that suggests that high [O III] $\lambda 5007$ + H$\beta$ line strengths may be a necessary condition for $f_{\text{esc}}$, but are by no means sufficient to guarantee high $f_{\text{esc}}$. This is reflected in our galaxy sample as well, where galaxies with extremely high [O III] $\lambda 5007$ + H$\beta$ strengths do not all necessarily appear to be strong LyC leakers.

We also note here that given the volume limited nature of the spectroscopic galaxy survey data used in this study, and the rarity on the sky of extreme line emitting galaxies, we are likely to miss several extreme [O III] $\lambda 5007$ + H$\beta$ line emitters in our sample. Studies investigating correlations between $f_{\text{esc}}$ and strength of [O III] $\lambda 5007$ + H$\beta$ emission (or [O III]/[O II] ratios) have largely focused on galaxy samples at relatively low redshifts, and the lack of completeness of extreme line emitters that are likely to exhibit high $f_{\text{esc}}$ is a caveat of any attempt to investigate the dependence of $f_{\text{esc}}$ on [O III] $\lambda 5007$ + H$\beta$ strength at $z > 3$ from our data set.

Therefore, our analysis has found a weak negative correlation between $f_{\text{esc}}$ and stellar mass, but contrary to expectations of models of reionisation, we do not see any significant correlation between $f_{\text{esc}}$ and specific SFR of galaxies. We have also found that only a small fraction ($\approx 6\%$) of galaxies in our sample can be reliably classified as candidate LyC leakers, although the uncertainties on the measured $f_{\text{esc}}$ are large owing to low significance of the measured LyC flux. The question that naturally arises following these findings, and is paramount to understanding the nature of sources in the early Universe that drove the bulk of reionisation, is: What regulates $f_{\text{esc}}$ in a galaxy? We discuss the relevance and implications of our findings in the following section.

6 DISCUSSION – WHAT REGULATES $f_{\text{esc}}$?

The escape fraction of ionising photons from star-forming galaxies crucially depends on the fraction of ionising radiation absorbed/scattered by the neutral gas and dust around the photon emitting regions. To have high $f_{\text{esc}}$, a large amount of neutral gas and dust must have been expelled from the star-forming regions through either supernova or AGN feedback (e.g. Wise et al. 2014; Trebitsch et al. 2017, 2018; Barrow et al. 2020; Katz et al. 2020). Given the dependence of high $f_{\text{esc}}$ from star-forming galaxies on the presence of ionised channels through which LyC photons can escape into the IGM, the orientation of the galaxies and potential (mis)alignment of these channels with the observer will play a key role in whether or not a galaxy appears to be leaking LyC radiation (e.g. Borthakur et al. 2014).

Therefore, by selection only a fraction of intermediate redshifts reionisation era analogue galaxies in any given sample will be identified as LyC leakers, assuming that these galaxies uniformly leak non-zero fractions of LyC photons. This geometrical misalignment of the viewing angles of a majority of sources may explain the relatively low numbers of individual galaxies identified in our sample, and across other samples that appear to be leaking significant fractions of LyC photons (e.g. Fletcher et al. 2019). A further explanation to the relatively low $f_{\text{esc}}$ values seen in the more relatively massive star-forming galaxies at intermediate redshifts could be the higher metallicities compared to the ultra-low metallicities expected from galaxies in the reionisation era (Yoo et al. 2020).

Another important factor that has an impact on whether or not a galaxy selected from a large sample appears to be a LyC leaker is the stochasticity of the IGM along the line-of-sight. Using ensembles of simulated IGM transmission functions along multiple lines-of-sight at $z \gtrsim 3$, Bassett et al. (2021) showed that for a given underlying
distribution of LyC $f_{\text{esc}}$ in a galaxy sample, only those galaxies that lie along sightlines with higher IGM transmission appear to be leaking LyC radiation, exhibiting high $f_{\text{esc}}$. Inclusion of a possible IGM transmission bias for both candidate LyC leakers and non leakers in this work may result in reduced $f_{\text{esc}}$ values for the leakers, with an increase in the upper limits of $f_{\text{esc}}$ inferred from stacking the non-leakers (e.g. Bassett et al. 2021).

In addition to observational effects such as orientation or stochastic IGM transmission, theoretical modelling has also revealed complex relationships between stellar population properties such as metallicity, ionisation parameter, etc. and $f_{\text{esc}}$, which impact the observed $f_{\text{esc}}$ and its dependence on physical properties of stars in a star-forming galaxy (e.g. Bassett et al. 2019). Further complexities are introduced by geometrical and viewing angle effects that further impact correlations between $f_{\text{esc}}$ and the strength of the ionising radiation field and ionising photon production rates from young stars traced by strong [O iii] + Hβ line strengths (e.g. Katz et al. 2020), among other galaxy properties. Barrow et al. (2020) showed that the periods during which a galaxy exhibits intense star-formation activity and ionising photon production, and periods corresponding to high $f_{\text{esc}}$ may be non-coincident, with high periods of $f_{\text{esc}}$ often following starburst activity (see also Kimm & Cen 2014; Trebitsch et al. 2017; Kakiichi & Gronke 2021).

However, it is important to note that conditions enabling high $f_{\text{esc}}$ following a starburst event may not necessarily coincide with an equally high production rate or efficiency of ionising photons ($\xi_{\text{ion}}$), as also seen in the simulations of Barrow et al. (2020). Therefore, there is an element of fortuitousness introduced in whether or not a star-forming galaxy selected from a large sample at any given epoch appears to be leaking LyC photons, and crucially depends on periods of both high $\xi_{\text{ion}}$ as well as high $f_{\text{esc}}$ being coincident (see also Fletcher et al. 2019; Nakajima et al. 2020).

Further, a spatially resolved analysis of the lensed LyC leaker dubbed ‘Sunburst’ at $z = 2.37$ (Dahle et al. 2016; Rivera-Thorsen et al. 2019) recently showed that a young massive star cluster dominates the leaking LyC radiation from the entire galaxy ($f_{\text{esc}} = 0.43 - 0.93$), whereas older clusters show considerably lower LyC $f_{\text{esc}}$ values (Vanzella et al. 2021). Without magnification due to lensing, the spatially unresolved Sunburst arc would exhibit a much lower LyC leakage overall ($f_{\text{rel}} = 0.06 - 0.12$) as the LyC radiation escaping along other lines of sight would be missed due to insufficient LyC imaging depths (see also Vanzella et al. 2020).

Therefore, in a scenario where a large fraction of LyC photons produced by only a limited number of individual young star clusters within galaxies manage to escape into the IGM through favourably aligned channels, there would be increased scatter in the observed dependence of $f_{\text{esc}}$ and galaxy properties such as stellar mass or specific SFR for any given sample of galaxies. Although this would explain the lack of significant correlations observed between $f_{\text{esc}}$ and the physical properties of candidate LyC leakers in this study, most importantly with the sSFR, such an effect complicates the observational understanding of what regulates the escape of ionising photons and consequently, which sources were the key drivers of reionisation. This makes studying indicators that trace the presence of LyC photons escape channels and their dependence on key galaxy properties crucial to understanding the physical and geometrical conditions that enable a high apparent $f_{\text{esc}}$ in the epoch of reionisation (e.g. Steidel et al. 2018).

One such probe is the Lyα line, whose shape, width and intensity can offer insights into LyC and Lyα escape channels from clusters of young stars within high redshift galaxies (e.g. Vanzella et al. 2018, 2020; Verhamme et al. 2017; Izotov et al. 2018a,b; Matthee et al. 2018; Meyer et al. 2021; Naidu et al. 2021). Additional high ionisation emission lines like He ii λ1640, C iv λ1548, 1550 and C iii] λ1907, 1909 in the rest-UV may help trace stellar populations that produce copious amounts of ionising photons, possibly leading to higher $f_{\text{esc}}$ (e.g. Schaerer et al. 2018; Berg et al. 2019; Scheney et al. 2019; Llerena et al. 2021). Saxena et al. (2020b) investigated He ii emitting star-forming galaxies in the redshift range $z = 2.5 - 5$ and did not find any strong dependence of the presence or the strength of He ii emission on the stellar mass or star-formation rates of galaxies (see also Nanayakkara et al. 2019), which may be consistent with factors that lead to a lack of observed dependence of $f_{\text{esc}}$ on these properties as discussed above.

A key advantage of our galaxy sample at $z \approx 3 - 3.5$ is the availability of rest-frame UV spectra from various spectroscopic surveys, crucially also covering the Lyα emission line, and in a future study we will explore the correlations between $f_{\text{esc}}$, Lyα and other rest-UV spectroscopic indicators for these newly discovered candidate LyC leakers (and non-leakers). JWST will give access, for the first time, to the full suite of rest-frame optical emission lines in $z > 3$ galaxies, enabling direct measurements of the ionising radiation field strengths produced by young stars (through [O ii] line strengths and [O iii]/[O ii] ratios) as well as measurements of the ionising photon production efficiencies using Hr measurements, which will considerably aid in identifying physical conditions within star-forming galaxies that lend themselves to high $f_{\text{esc}}$. The correlations between $f_{\text{esc}}$ and rest-frame optical emission established at these intermediate redshifts will be instrumental in interpreting the ionising photon escape of galaxies at $z = 6 - 9$, for which JWST will enable rest-optical spectroscopy, in a bid to understand the nature of the main drivers of reionisation.

Therefore, going forward it is essential to obtain deeper LyC imaging for intermediate redshift analogues of reionisation era galaxies to properly account for the viewing angle and orientation effects when measuring $f_{\text{esc}}$. Further, detailed studies of the rest-frame UV and optical spectra of known LyC leakers are needed to investigate the presence of LyC escape channels and study the dependence of these features on galaxy properties. Better insights into the timescales and the incidence of high $f_{\text{esc}}$ within star-forming galaxies may be needed from high-resolution simulations (e.g. Mauerhofer et al. 2021) of a larger number of reionisation era galaxies (with sufficient time resolution) to temporally tie periods of intense star-formation to $f_{\text{esc}}$ and other galaxy properties.

7 SUMMARY AND CONCLUSIONS

We have measured the Lyman continuum (LyC) escape fraction ($f_{\text{esc}}$) using ground based LyC images available for 183 spectroscopically confirmed galaxies in the CDFS/GOODS-S field in the redshift range 3.11 < $z < 3.53$. The spectroscopic redshifts are taken from publicly available databases, that primarily targeted the higher mass Lyman break (LBG) selected galaxies or blindly discovered lower mass galaxies thanks to emission line surveys.

We use available deep HST photometry and colours at non-ionising UV wavelengths to remove possible foreground contaminants that may strongly bias the inferred LyC flux and $f_{\text{esc}}$ as well as accurately constrain the spectral energy distributions (SEDs) of our galaxies giving robust measurements of key galaxy properties. Using a combination of stellar and nebular emission, we also derive rest-frame optical emission line strengths, primarily the [O iii] and Hβ line fluxes (that fall in the observed K band) for our galaxies.

We then measure LyC flux and $f_{\text{esc}}$ using aperture photometry and

MNRAA 000, 1–18 (2021)
detect LyC flux at $\geq 2\sigma$ significance levels in 11 out of 183 galaxies, with $f_{\text{esc}}$ values ranging from 0.14–0.85. Around 94% of the galaxies in our sample remain undetected at the $\geq 1\sigma$ level, and using weighted averaging of their LyC $f_{\text{esc}}$ limits, we place a 1$\sigma$ upper limit of $f_{\text{esc}} < 0.12$ from the galaxies with no significant detections in the available LyC images. We additionally compare the weighted average $f_{\text{esc}}$ limits from sub-samples of galaxies that were LBG or blind-selected, finding 1$\sigma$ limits of $f_{\text{esc}} < 0.11$ for LBG-selected and $f_{\text{esc}} < 0.13$ for blind-selected galaxies. We further place $f_{\text{esc}}$ limits from normal emission line galaxies (ELGs; [O\textsc{ii}]) and extreme emission line galaxies (EELGs; [O\textsc{ii}]+H\textbeta) and extreme emission line galaxies (EELGs; [O\textsc{ii}]+H\textbeta > 300 Å), finding 1$\sigma$ limits of $f_{\text{esc}} < 0.14$ for normal and $f_{\text{esc}} < 0.20$ for extreme emission line galaxies.

Although the uncertainties on the measured $f_{\text{esc}}$ values for the 11 candidate LyC leaking galaxies are high and a handful of sources have low signal-to-noise ratios in the LyC images ($\approx 2\sigma$), we find a weak negative correlation between $f_{\text{esc}}$ and stellar mass at the $\geq 2\sigma$ level, with a shallow slope of $-0.10 \pm 0.02$. We do not find any significant correlation between $f_{\text{esc}}$ and specific star-formation rate of the individual LyC leakers at the $\geq 2\sigma$ level, with a slope of $-0.028 \pm 0.015$. Lastly, we find a positive correlation between $f_{\text{esc}}$ and EW$_{\text{[O\textsc{ii}]+H\textbeta]}$ for the candidate LyC leakers in our sample, suggesting that the [O\textsc{ii}]+H\textbeta line strengths may be important indicators of $f_{\text{esc}}$ as has been previously reported in the literature.

From our results, it remains unclear what the dominant galaxy property is when it comes to regulating $f_{\text{esc}}$ in LyC leaking galaxies. The low detection fraction of LyC leakers across our sample is consistent with a scenario where LyC photons escape through discrete ionised channels within star-forming galaxies, which are seldom oriented along the line-of-sight of the observer. The time-dependent nature of high $f_{\text{esc}}$ that often follows periods of intense star-formation also suggests that only a low fraction of galaxies at any given epoch would be actively leaking LyC photons, consistent with our observations.

The stochasticity of the intervening neutral intergalactic medium, which may play an important role in absorbing leaking LyC photons along the line-of-sight is another factor that may impact LyC detections. Future work tying LyC escape to the presence of ionised channels within galaxies using observations, exploration of the time-dependent nature of LyC leakage from larger samples of simulated reionisation era galaxies as well as investigation of IGM stochasticity across redshifts are needed to fully understand these effects in the context of contribution of star-forming galaxies towards the cosmic reionisation photon budget.

In conclusion, our work has discovered a sample of 11 previously undiscovered candidate LyC leakers at $z \sim 3 - 3.5$ adding crucial statistics that are needed to understand the escape of ionising photons from intermediate redshift analogues of $z > 6$ galaxies. Studying lower redshift analogues of reionisation era galaxies, where direct detection of escaping LyC radiation is possible, remains the only way to constrain LyC escape from star-forming galaxies that are expected to drive the bulk of reionisation. An increased sample of LyC leaking galaxies complemented by deeper LyC/UV imaging, higher resolution spectra across wavelengths and zoom-in simulations will help understand the unique physical conditions that drive high $f_{\text{esc}}$, bringing us a step closer towards unravelling the nature of galaxies and their ionising radiation that drove cosmic reionisation.

**ACKNOWLEDGEMENTS**

We thank the referee for constructive feedback that improved the quality of this work. AS thanks Ross McLure and Mario Nonino for useful input and discussions, Fergus Cullen for sharing NIRVANDELS measurements and Mengtao Tang for sharing the best-fitting relation for emission line strengths from their analysis. AS and LP thank Alice Shapley for useful comments and discussions that improved the analysis presented.

AS and RSE acknowledge financial support from European Research Council Advanced Grant FP7/669253. DS and ASL acknowledge support from Swiss National Science Foundation. RA acknowledges support from ANID FONDECYT Regular 1202007. MLI acknowledges support from the National Agency for Research and Development (ANID)/Scholarship Program/Doctorado Nacional/2019-21191036.

This work makes use of VANDELS data. The VANDELS collaboration acknowledges the invaluable role played by ESO staff for successfully carrying out the survey. This work is based on VUDS data, obtained with the European Southern Observatory Very Large Telescope, Paranal, Chile, under Large Program 185.A-0791, and made available by the VUDS team at the CESAM data center, Laboratoire d’Astrophysique de Marseille, France. This work is based on observations taken by the MUSE-Wide and MUSE-HUDF Surveys as part of the MUSE Consortium. This work is based on observations taken by the 3D-HST Treasury Program (GO 12177 and 12328) with the NASA/ESA HST, which is operated by the Association of Universities for Research in Astronomy, Inc., under NASA contract NAS5-26555. MLI acknowledges support from the National Agency for Research and Development (ANID)/Scholarship Program/Doctorado Nacional/2019-21191036.

This work has made extensive use of Jupyter and IPython (Pérez & Granger 2007) notebooks, Astropy (Astropy Collaboration et al. 2013, 2018), matplotlib (Hunter 2007), seaborn (Waskom & the seaborn development team 2020), pandas (pandas development team 2020) and TOPCAT (Taylor 2005). This work would not have been possible without the countless hours put in by members of the open-source developing community all around the world, with special thanks to the Stackoverflow community.

**DATA AVAILABILITY**

The VANDELS data can be accessed using the VANDELS database at http://vandels.inaf.it/dr4.html, or through the ESO archives. The VUDS data can be accessed from the VUDS webpage: http://cesam.lam.fr/vuds/ or ESO archives. MUSE data can be accessed from https://musewide.aip.de/project/ and http://muse-vlt.eu/science/udf/ and the 3D-HST data can be accessed from https://archive.stsci.edu/prepsds/3d-hst/. The VIMOS10 data are available from Balestra et al. (2010). All the code used to perform the analysis in this paper was written in PYTHON and will be shared upon reasonable request to the corresponding author.

**REFERENCES**

Asplund M., Grevesse N., Sauval A. J., Scott P., 2009, ARA&A, 47, 481
Astropy Collaboration et al., 2013, A&A, 558, A33
Astropy Collaboration et al., 2018, AJ, 156, 123
Balestra I., et al., 2010, A&A, 512, A12
Shapley A. E., Steidel C. C., Strom A. L., Bogosavljević M., Reddy N. A., Siana B., Mostardi R. E., Rudie G. C., 2016, *ApJ, 826, L24*
Siana B., et al., 2007, *ApJ, 668, 62*
Siana B., et al., 2015, *ApJ, 804, 17*
Smit R., et al., 2015, *ApJ, 801, 122*
Smith B. M., et al., 2020, *ApJ, 897, 41*
Stark D. P., 2016, *ARA&A, 54, 761*
Stark D. P., Schenker M. A., Ellis R., Robertson B., McLure R., Dunlop J., 2013, *ApJ, 763, 129*
Stasińska G., Izotov Y., Morisset S., Guseva N., 2015, *A&A, 576, A83*
Steidel C. C., Pettini M., Adelberger K. L., 2001, *ApJ, 546, 665*
Steidel C. C., Bogosavljević M., Shapley A. E., Reddy N. A., Rudie G. C., Pettini M., Tranor R. F., Strom A. L., 2018, *ApJ, 869, 123*
Tang M., Stark D. P., Chevallard J., Charlton S., 2019, *MNRAS, 489, 2572*
Tasca L. A. M., et al., 2017, *A&A, 600, A110*
Taylor M. B., 2005, in Shopbell P., Britton M., Ebert R., eds, Astronomical Society of the Pacific Conference Series Vol. 347, Astronomical Data Analysis Software and Systems XIV, p. 29
Trebitsch M., Blaizot J., Rosdahl J., Devriendt J., Slyz A., 2017, *MNRAS, 470, 224*
Trebitsch M., Volonteri M., Dubois Y., Madau P., 2018, *MNRAS, 478, 5607*
Urrutia T., et al., 2019, *A&A, 624, A141*
Vanzella E., Siana B., Cristiani S., Nonino M., 2010, *MNRAS, 404, 1672*
Vanzella E., et al., 2016a, *ApJ, 821, L27*
Vanzella E., et al., 2016b, *ApJ, 825, 41*
Vanzella E., et al., 2018, *MNRAS, 476, L15*
Vanzella E., et al., 2020, *MNRAS, 491, 1093*
Vanzella E., et al., 2021, arXiv e-prints, p. arXiv:2106.10280
Verhamme A., Orlitová I., Schaerer D., Izotov Y., Worseck G., Thuan T. X., Guseva N., 2017, *A&A, 597, A13*
Waskom M., the seaborn development team 2020, mwaskom/seaborn, doi:10.5281/zenodo.592845, https://doi.org/10.5281/zenodo.592845
Wise J. H., Demchenko V. G., Halicek M. T., Norman M. L., Turk M. J., Abel T., Smith B. D., 2014, *MNRAS, 442, 2560*
Yoo T., Kimm T., Rosdahl J., 2020, *MNRAS, 499, 5175*
Zackrisson E., Inoue A. K., Jensen H., 2013, *ApJ, 777, 39*
de Barros S., et al., 2016, *A&A, 585, A51*
pandas development team T., 2020, pandas-dev/pandas: Pandas, doi:10.5281/zenodo.3509134, https://doi.org/10.5281/zenodo.3509134

**APPENDIX A: Lyc AND HST CUTOUT GALLERIES WITH BEST-FITTING SEDS OF CANDIDATE Lyc LEAKERS**

This paper has been typeset from a TeX/LaTeX file prepared by the author.
Figure A1. Continued.