Abstract—This paper summarizes our attempts to establish a systematic approach that overcomes a key difficulty in sensing wireless microphone signals, namely, the inability for most existing detection methods to effectively distinguish between a wireless microphone signal and a sinusoidal continuous wave (CW). Such an inability has led to an excessively high false alarm rate and thus severely limited the utility of sensing-based cognitive transmission in the TV white space (TVWS) spectrum. Having recognized the root of the difficulty, we propose two potential solutions. The first solution focuses on the periodogram as an estimate of the power spectral density (PSD), utilizing the property that a CW has a line spectral component while a wireless microphone signal has a slightly dispersed PSD. In that approach, we formulate the resulting decision model as an one-sided test for Gaussian vectors, based on Kullback-Leibler distance type of decision statistics. The second solution goes beyond the PSD and looks into the spectral correlation function (SCF), proposing an augmented SCF that is capable of revealing more features in the cycle frequency domain compared with the conventional SCF. Thus the augmented SCF exhibits the key difference between CW and wireless microphone signals. Both simulation results and experimental validation results indicate that the two proposed solutions are promising for sensing wireless microphones in TVWS.

I. INTRODUCTION

The digital TV transition has created the opportunity of realizing cognitive radio in the TV white space (TVWS) spectrum [1]-[3]. In the envisioned TVWS systems, TV band devices (TVBDs) cognitively operate in TV spectrum that is not used by TV broadcasting services or certain low-power auxiliary stations such as wireless microphones [4].

Spectrum sensing is a functionality for TVBDs, via signal processing techniques, to identify the presence or absence of TV or wireless microphone signals with high reliability, thus providing an effective protection mechanism for those incumbent services. While sensing for TV signals such as ATSC/NTSC/DVB-T has been demonstrated as feasible [5]-[8], sensing for wireless microphone signals remains a challenging problem. Most tested sensing prototypes have not exhibited satisfactory performance, especially in realistic environment [5].

There have been a number of works [9]-[15] aiming at improving the accuracy of wireless microphone sensing. Among those works, despite of their different methodologies, a common ingredient is that the background noise is modeled as Gaussian, either white, or colored in the presence of adjacent channel interference. Since wireless microphone signal is a narrowband frequency-modulated (FM) waveform [4], its power spectral density (PSD) or (the magnitude of) spectral correlation function (SCF) manifests itself like one or several peaks in the perceptually “smooth” noise background. Visually, such a situation is like “telling the tree from the grassland”.

In realistic environment, however, the perhaps unpleasant reality is that the background noise is seldom pure Gaussian. As is well known, narrowband interference such as spurious emissions, unintentional transmissions, leakage, and inter-modulation are inevitable and universal in electronic devices. Available regulatory rules do strictly limit their interference upon communications. For spectrum sensing which is supposed to be capable of detecting weak signals well below the noise floor, however, the impact of those narrowband interference sources becomes crucial. Figure [1] illustrates such a situation.

In retrospect, the main difficulty with wireless microphone sensing has been largely related to such narrowband interference, which “fools” sensing algorithms to erroneously report that an available TVWS is being used, thus incurring excessively high false alarm rate and severely reducing the amount of sensed TVWS spectrum. This difficulty has been realized by researchers mainly from the industry side [7],[16],[17]. The foremost task, therefore, is to distinguish between an FM wireless microphone signal and a sinusoidal continuous wave (CW) which models the narrowband interference, and the situation thus is more like “telling the wheat from the chaff”, in that it is necessary to extract fine features of the received signal in order to make the correct decision.

Recently, the sensing prototype reported in [8] used an ad hoc algorithm to decide whether a received narrowband signal is from a wireless microphone or is a CW from an interference source. The algorithm computes certain features of the periodogram of the received signal, and tests those features against rules that have been fine-tuned via training several specific makes of wireless microphones. In the current paper, we attempt to establish a more systematic understanding of the underlying decision problem, and upon such a understanding, develop more systematic sensing methods, that are potentially suited for general scenarios without extensive training and fine-tuning. Specifically, we focus on
two approaches that are based on the periodogram and an augmented SCF, respectively. The first approach focuses on the periodogram, which is an estimate of the PSD, utilizing the property that a CW has a line spectral component while a wireless microphone signal, as FM, has a slightly dispersed PSD. We formulate the resulting decision model as an one-sided hypothesis test for Gaussian vectors, and develop the decision statistic based on the Kullback-Leibler distance between the empirical distribution of the observed periodogram and the distribution of the periodogram under CW hypothesis. The second approach goes beyond the PSD and looks into the SCF. More specifically, we propose to use an augmented SCF that combines the conventional SCF and a proposed conjugate SCF. The augmented SCF is capable of revealing more features in the cycle frequency domain compared with the conventional SCF, and thus exhibits the key difference between CW and wireless microphone signals. As both simulation results and experimental validation results indicate, the two proposed approaches are promising solutions for sensing wireless microphones in TVWS.

Some remarks on the relevance of the topic are in order. The Federal Communication Commission (FCC) of the United States recently has waived the mandatory requirements on spectrum sensing, turning to geolocation database access as the main means of primary service protection for TVWS systems [1]. However, this change in the policy should not be deemed as the end of TVWS spectrum sensing. First, the FCC rules still encourage further research into spectrum sensing and keep the option of “sensing only” TVBDs, which sometimes may be more flexible to use than TVBDs that use only geolocation database access. The sensing threshold for wireless microphone signals in the FCC rules is set as $-107$ dBm, which, when considering a 6 MHz TV channel of background thermal noise only and a typical handset RF circuitry implementation [8], would correspond to a signal-to-noise ratio (SNR) lower than $-10$ dB. Second, in a deployed geolocation database service, it will be useful or even necessary for the administrators to have some TVBDs or some surveillance nodes possess the sensing capability, so that they can, when needed, verify the validity of records in the database. Third, the understanding we develop herein for wireless microphone sensing may prove useful under other scenarios, say, cognitive radio in TVWS of other countries, or in other spectrum bands for cognitive usage.

The remaining part of this paper is organized as follows. Section II formulates the decision-theoretic model of wireless microphone sensing. Sections III and IV respectively develop the sensing approaches based on the periodogram and an augmented SCF of the received signals, describe the sensing methods, and present their performance by simulations. Section V presents the experimental validation of the two approaches. Section VI concludes the paper.

II. Problem Formulation

Since a wireless microphone may choose its carrier frequency rather flexibly, upon receiving the signals from a TV channel, the first task is to identify the frequency location(s) of potential wireless microphone signal(s). To accomplish this task, a simple and effective method (see, e.g., [6][8]) is to compute the periodogram of the signal, scan through the periodogram to search for peaks that exceed a certain prescribed threshold. In order to focus our attention on the core problem, we assume that the frequency scan has been done successfully, and that for each thus identified spectral peak, the resulting binary hypothesis testing problem is

$$H_1 \text{ (wireless microphone)} : \quad x(t) = A \cos \left( 2\pi f_c t + 2\pi \beta \int_0^t m(\tau) d\tau + \varphi \right) + w(t), \quad (1)$$

$$H_0 \text{ (CW)} : \quad x(t) = A \cos(2\pi f_c t + \varphi) + w(t). \quad (2)$$

In the problem formulation, $A$ denotes the carrier magnitude, $f_c$ denotes the carrier frequency, and $\varphi$ denotes the signal phase uncertainty, which may be deemed as uniformly distributed in $[0, 2\pi]$. For the FM wireless microphone signal, $m(t)$ represents the message which may be the voice of the speaker, and $\beta$ is the frequency deviation, whose value determines the degree of dispersion of the resulting FM spectrum. The noise $w(t)$ is modeled as zero-mean white noise.
Gaussian, and in this paper we do not consider the issue of colored noise due to adjacent channel leakage. Inspecting the problem formulation, we clearly see that its key distinction from the existing works is that the null hypothesis $H_0$ is no longer pure Gaussian noise, but contains a CW component, which closely captures the ambiguity due to the narrowband interference encountered in realistic TV channels [7][17][8]. In reality, however, since the prior statistical knowledge of $m$ is unavailable, and the signal part is typically weak compared to down-converting, low-pass filter, and sample $x(t)$. Denote by $f_s$ the sampling rate for low-pass filtered baseband signal, and let $T_s = 1/f_s$. We have the discrete-time version of the hypothesis testing problem (1) (2) as the estimate of the PSD. Due to the central limit theorem, this difficulty thus motivates our idea of using one-sided test. That is, we only specify the statistics of $\xi_a$ under both $H_0$ and $H_1$, which has proven effective in both simulation and experiments.

### III. Periodogram-based Solution

#### A. Rationale of Using Periodogram and One-sided Test

The periodogram is an estimate of the PSD of the received signal embedded in noise. The starting point of using periodogram here is a well-known fact that, CW has a line PSD whereas a wireless microphone signal has a slightly dispersed PSD due to the modulation by the message $m(t)$. So extracting fine features of the periodogram will enable the detector to distinguish between CW and wireless microphone.

The approach we take in this work, unlike the ad hoc approach in [8] where “behavioral” features like main lobe width are extracted from the periodogram to form the decision statistics, treats the periodogram as a vector of Gaussian random variables and establishes the decision rule based on such a Gaussian model. Concretely, for $M$ non-overlapping length-$N$ segments of the received signals, we compute their averaged periodogram, denoted by $\xi_a = (\xi_a[0], \xi_a[1], \ldots, \xi_a[N-1])$, as the estimate of the PSD. Due to the central limit theorem, for moderate or large $M$ we may approximate $\xi_a$ as a vector of Gaussian random variables. Hence if we could obtain the means and covariances of $\xi_a$ under both $H_0$ and $H_1$, we could directly utilize the likelihood ratio test to decide whether a received signal is a CW or a wireless microphone signal.

A realistic difficulty with likelihood ratio tests, unfortunately, is that the mean and covariance of $\xi_a$ is generally unknown under $H_1$, due to the lack of prior knowledge on the FM implementation details of wireless microphones. Different makes of wireless microphones may have quite different implementations. Their choices of the frequency deviation $\beta$ differ and the statistics of $m(t)$ highly depend on the message characteristics and the audio processing methods. This difficulty thus motivates our idea of using one-sided test. That is, we only specify the statistics of $\xi_a$ under the null hypothesis $H_0$, and the one-sided test aims at telling whether a received signal is from $H_0$ or not. Whenever it is decided that the null hypothesis is to be rejected, we interpret the rejection as an indication of the occurrence of wireless microphone signals.

There are numerous one-sided test rules, and in this work, we follow the information-theoretic approach in [19], using the Kullback-Leibler (KL) distance between the empirical distribution of the averaged periodogram and the actual distribution of $\xi_a$ under $H_0$. The idea is that since the KL distance vanishes only if its two distributions coincide, we would accept the null hypothesis only when the KL distance is sufficiently small. A side note is that one may also use other, perhaps more refined, PSD estimates to replace periodogram in computing the statistics. We, however, do not expect that refinement to yield significant performance improvement. There are two considerations. First, the lack of prior statistical knowledge for wireless microphone signals prevents the usage of many data-dependent, parametric PSD estimation methods. Second, most nonparametric PSD estimation methods tend to “fatten”...
the main lobe of signals, thus rendering it more difficult to distinguish CW from wireless microphone signals.

B. Method Description

Regarding the signal model of CW in (4), in Appendix VI-A we evaluate the means and variances of its periodogram. Specifically, since the frequency offset is eliminated and $M$ periodograms are averaged, we have from (18) and (19) that

$$
\begin{align*}
\mu[k] &\triangleq \mathbb{E}\{\xi[k]\} = \sigma^2(N \cdot \text{SNR} + 1) \quad \text{if } k = 0 \\
&= \sigma^2 \quad \text{otherwise} \\
\eta[k,k] &\triangleq \text{var}\{\xi[k]\} = \frac{\sigma^4}{M} \left(2N \cdot \text{SNR} + 1\right) \quad \text{if } k = 0 \\
&= \frac{\sigma^4}{M} \quad \text{otherwise}. \quad (5)
\end{align*}
$$

Furthermore, without frequency offset, we can directly verify that the off-diagonal elements $\{\eta[k,l]\}_{k \neq l}$ in the covariance matrix of $\xi$ are all zero. Denote the mean vector of $\xi$ by $\mu = (\mu[0], \mu[1], \ldots, \mu[N-1])$, and the covariance matrix of $\xi$ by

$$
\eta = \begin{bmatrix}
\eta[0,0] & 0 & \cdots & 0 \\
0 & \eta[1,1] & \cdots & 0 \\
\vdots & \vdots & \ddots & \vdots \\
0 & 0 & \cdots & \eta[N-1, N-1]
\end{bmatrix}.
$$

So by our approximation, $\xi \sim \mathcal{N}(\mu, \eta)$. On the other hand, upon computing the averaged (over $M$ non-overlapping length-$N$ segments) periodogram of the received signal, which may be either a CW or a wireless microphone signal, we can evaluate its empirical mean and covariance. Denote by $\hat{\xi}$ the empirical averaged periodogram, and by $\hat{\mu}_e$ and $\hat{\eta}_e$ its empirical mean vector and covariance matrix respectively. According to the one-sided decision rule using KL distance [19], the decision statistic is given by

$$
T_{p,0} \triangleq \mathbb{D}(\mathbb{N}(\mu_e, \eta_e)\|\mathbb{N}(\mu, \eta)) = \frac{1}{2}(\mu_e - \mu)^T \eta_e^{-1} (\mu_e - \mu) + \frac{1}{2} \left[ \text{trace}(\eta_e^{-1} - I) + \log \frac{\det \eta_e}{\det \eta} \right]. \quad (7)
$$

In $T_p$ we need to compute the empirical covariance matrix $\eta_e$ and use all the $N$ elements of $\hat{\xi}$. Both of these practices are computation-intensive and usually sensitive to outliers in real data. Therefore, in order to simplify the detector implementation and to improve its immunity to outliers, we use in this work the following decision statistic,

$$
T_p \triangleq \frac{1}{2}(\mu_{e,L} - \mu_L)^T \eta_L^{-1} (\mu_{e,L} - \mu_L), \quad (8)
$$

where $L \leq N$ is a window size, $\mu_L = (\mu[0], \mu[1], \ldots, \mu[L-1])$, $\mu_{e,L} = (\mu_{e,0,0}, \mu_{e,1,1}, \ldots, \mu_{e,L,L-1})$, and $\eta_L$ is the submatrix of $\eta$ formed by its first $L$ rows and first $L$ columns.

Given a threshold $\gamma$, the decision rule is as follows,

$$
\mathcal{H} = \mathcal{H}_0 \quad \text{if } T_p \leq \gamma; \quad \text{and } \mathcal{H}_1 \quad \text{otherwise.}
$$

By adjusting $\gamma$ we control the false alarm rate. This needs to be accomplished by the aid of Monte Carlo simulations. A first-cut approximation may be used for not too small target false alarm rates, based on the Gaussian approximation of $\xi$. That is, from the decision statistic in (8), when the Gaussian approximation is well-satisfied, we have $T_p \sim \chi^2(L)$.

C. Simulation Results

We use Monte Carlo simulation to verify our periodogram-based sensing method. We generate bandpass CW and FM wireless microphone signals contaminated by white Gaussian noise, then down-convert, low-pass filter, and down-sample the signals to obtain the baseband discrete-time signals as in (3) and (4). The SNR is set with respect to a 8MHz bandwidth (the TV channels in China are 8MHz), and varies between $-15$dB and $-23$dB. For simplicity and generality, when generating FM wireless microphone signals, we let the message $m(t)$ be a Brownian motion. For making decision, fifteen segments of signals each of time duration 10ms are used to generate the decision statistics.

In our simulation, we mainly aim at revealing the impact of the following three key parameters:

- SNR
- $L$: the window size when computing $T_p$
- $\beta$: the frequency deviation in FM wireless microphone signals

Figure 2 displays the receive operating characteristic (ROC) curves of the detection method, for $L = 11$, $\beta = 0.7$, under different values of SNR. The x-axis is the false alarm rate and the y-axis is the corresponding detection rate (or, one minus the miss rate). It is clearly seen that increasing the SNR dramatically improves the detector performance. When the SNR is (or higher than) $-21$dB, the detection rate exceeds 98% with the false alarm rate being 5%.

Figure 3 displays the ROC curves for SNR = $-17$dB, $\beta = 0.7$, under different values of $L$. It is seen that the detector performance improves with $L$, thus indicating the tradeoff between performance and complexity. Furthermore, increasing $L$ beyond 11 does not appear to yield substantial performance gain. For $L = 5$, the detection rate exceeds 98% with the false alarm rate being as low as 1%.

Figure 4 displays the ROC curves for SNR = $-17$dB, $L = 11$, under different values of $\beta$. It is seen that the detector performance improves with $\beta$, which is consistent with the features of the periodogram of wireless microphone. Furthermore, for the values of $\beta$ beyond 0.5, the detection rate exceeds 98% with the false alarm rate being as low as 1%.

IV. AUGMENTED SCF-BASED SOLUTION

A. Preliminary of SCF

The SCF was originally proposed to reveal the cyclostationarity embedded in a signal, when its spectral components are
temporally correlated \[20\] \[21\] \[22\]. The SCF of a continuous-time signal \(x(t)\) is defined as \[20\]

\[
S^\alpha_x(f) \triangleq \lim_{T \to \infty} \lim_{\Delta t \to \infty} S^\alpha_{X_T}(f) \Delta t,
\]

\[
S^\alpha_{X_T}(f) \Delta t \triangleq \frac{1}{T \Delta f} \int_{-\Delta f}^{\Delta f} X_T(t, f + \alpha/2) X^*_T(t, f - \alpha/2) dt,
\]

\[
X_T(t, f) \triangleq \int_{t-T/2}^{t+T/2} x(u) e^{-j2\pi fu} du,
\]

where \(\alpha\) denotes the cycle frequency. Intuitively, the SCF \[9\] measures the normalized correlation between two spectral components of \(x(t)\) at frequencies \(f + \alpha/2\) and \(f - \alpha/2\) over a length-\(\Delta t\) time interval.

Given a sequence of discrete-time samples of signal \(x[n], n = 1, 2, \ldots, N - 1\), a simple approximation of the SCF \(S^\alpha_x(f)\) may be computed as \[20\] \[23\]

\[
\hat{S}^\alpha_x(f) \triangleq \frac{1}{MN} \sum_{k=-(M-1)/2}^{(M-1)/2} X(f + k/N + \alpha/2) X^*(f + k/N - \alpha/2),
\]

where \(M \leq N\) is an odd positive integer determining the frequency resolution \(\Delta f = M/N\) of the estimate, and \(X(f)\) is the discrete-time Fourier transform (DTFT) of \(x[\cdot]\),

\[
X(f) \triangleq \sum_{n=0}^{N-1} x[n] e^{-j2\pi fn}.
\]

For efficiency, the computation of \(\hat{S}^\alpha_x(f)\) is usually implemented by a fast Fourier transform (FFT) algorithm, over all of the values of \(f\) such that \(f \pm \alpha/2\) are integer multiples of \(1/N\).

Most digitally modulated signals exhibit a certain degree of cyclostationarity, and have distinctive patterns in their SCFs. Stationary Gaussian noise, however, shows no cyclostationarity, so that for any \(\alpha \neq 0\) its SCF is nearly zero. Therefore, methods based on SCF have been widely used for modulated signal detection and classification \[21\].

B. Conjugate SCF and Augmented SCF

When we apply SCF to CW and wireless microphone signals, a potential problem arises; that is, the SCF for \(\alpha \neq 0\) is usually too weak to render any extractable feature for detection. This phenomenon may be illustrated by examining the SCF of a sampled bandpass CW: \(x[n] = A \cos(2\pi f_c T_s n + \varphi)\). We denote \(f_c T_s\) by \(f_0\) as the normalized carrier frequency in discrete-time. For such a signal, its DTFT \[11\] computed using
Now in order to exhibit more features on the \((\alpha, f)\)-plane for the purpose of detection, we propose to introduce the concepts of conjugate SCF and augmented SCF. The idea of conjugate SCF is simply swapping the role of \(f\) and \(\alpha\), to define
\[
\hat{S}_x^\alpha(f)_c \triangleq \frac{1}{MN} \sum_{k=-(M-1)/2}^{(M-1)/2} X(f + \frac{k}{N} + \frac{\alpha}{2}) \cdot X^\dagger(f - \frac{k}{N} - \frac{\alpha}{2})
\]
where the subscript \(c\) represents “conjugate”. The reader may compare its difference from the definition of the SCF (10). Compared with SCF, The conjugate SCF appears to exhibit more features along the \(\alpha\) axis. For the sampled bandpass CW example examined above, the following four locations on the \((\alpha, f)\)-plane possibly exhibit sharp conjugate SCF feature peaks:

1) \(f = 0\), values of \(\alpha\) in the vicinity of \(\alpha \in [2f_0 - \frac{M-1}{2N}, 2f_0 + \frac{M-1}{2N}]\) satisfying \(f \pm (k/N + \alpha/2) = \pm f_0\) for some integer \(k\);
2) \(f = 0\), values of \(\alpha\) in the vicinity of \(\alpha \in [-2f_0 - \frac{M-1}{2N}, -2f_0 + \frac{M-1}{2N}]\) satisfying \(f \pm (k/N + \alpha/2) = \mp f_0\) for some integer \(k\);
3) \(f = f_0\), values of \(\alpha\) in the vicinity of \(\alpha \in [-\frac{M-1}{N}, \frac{M-1}{N}]\) satisfying \(f \pm (k/N + \alpha/2) = f_0\) for some integer \(k\);
4) \(f = -f_0\), values of \(\alpha\) in the vicinity of \(\alpha \in [-\frac{M-1}{N}, \frac{M-1}{N}]\) satisfying \(f \pm (k/N + \alpha/2) = -f_0\) for some integer \(k\).

Now we further define the augmented SCF as
\[
\hat{S}_x^\alpha(f)_a \triangleq \kappa_1 \hat{S}_x^\alpha(f)|_{\alpha=0} + \kappa_2 \hat{S}_x^\alpha(f)_c|_{\alpha \neq 0},
\]
where the subscript \(a\) represents “augmented”. The weighting factors \(\kappa_{1,2}\) balance the impacts from SCF and the conjugate SCF. Note that, for SCF we only keep its components on \(\alpha = 0\), so indeed \(\hat{S}_x^0(f)\) is an estimate of the signal PSD; while for the conjugate SCF we ignore its components for \(\alpha = 0\). Such a definition of the augmented SCF here is specifically tailored to suit the problem of distinguishing between CW and wireless microphone signals, while other definitions are possible (and perhaps more appropriate) for more extensive potential applications. Figures 5 and 6 display the magnitudes of the augmented SCFs of a baseband CW and a baseband wireless microphone signal, respectively. In both figures we use the same set of weighting factors \(\kappa_{1,2}\). Visually we can notice the difference between the two augmented SCFs, in that the CW tends to have larger conjugate SCF magnitudes compared with the SCF at \(\alpha = 0\), while the wireless microphone signal shows an opposite behavior. A precise mathematical explanation of such a difference does not appear straightforwardly available, given our limited knowledge regarding the statistical properties of wireless microphone signals. In Appendix VI-B we sketch out a first-cut analysis which provides useful intuition about the underlying mechanism.
C. Method Description

Having noticed the visual difference between the augmented SCFs of a CW and a wireless microphone signal, we need to quantitatively convey such difference using a decision statistic. In this work, we choose to use the following statistic,

\[ T_a \triangleq 1 - \frac{\left| \sum_{\alpha \in \Omega} |\hat{S}_{\alpha}^a(f)_{\alpha}| \right|_{f=0}}{\left| \sum_{f \in \Psi} |\hat{S}_{\alpha}^a(f)_{\alpha}| \right|_{\alpha=0}}. \]  

(14)

Herein, \( \Psi \) is a window of frequency bins among which we average \( |\hat{S}_{\alpha}^a(f)_{\alpha}| \), and \( \Omega \) is a window of cycle frequency bins among which we average \( |\hat{S}_{\alpha}^a(f=0)_{\alpha}| \). So the statistic \( T_a \) is just one minus the ratio between the averaged augmented SCF magnitudes on \( f = 0 \) and the averaged augmented SCF magnitudes on \( \alpha = 0 \). From our visual observation, for CW, \( T_a \) tends to be small, while for wireless microphone signals, \( T_a \) tends to be large.

We remark that, in order to compute \( T_a \), we only need to compute the values of the SCF on \( \alpha = 0 \) (that is, the PSD) within window \( \Psi \), and the values of the conjugate SCF on \( f = 0 \) within window \( \Omega \). Without the need to compute the augmented SCF over the entire \((\alpha, f)\)-plane, the implementation complexity of the detection method may be moderate and suitable for practice.

Even under \( \mathcal{H}_0 \), the distribution of \( T_a \) is complicated to analyze. Hence we use Monte Carlo simulation to determine the decision threshold \( \gamma \), in order to meet a specified target false alarm rate. The decision rule is as follows,

\[ \hat{\mathcal{H}} = \mathcal{H}_0 \quad \text{if} \quad T_a \leq \gamma; \quad \text{and} \quad \mathcal{H}_1 \quad \text{otherwise.} \]

In order to combat against noise and thus improve the decision accuracy, the statistics of multiple separate segments of signals may be averaged or appropriately combined.

D. Simulation Results

The simulation setup is identical to that in Section III-C, except that for computing the augmented SCF the sampling rate is set as 20MHz. The weighting factors in \( \hat{S}_{\alpha}^a(f)_{\alpha} \) are chosen as \( \kappa_1 = 0.1 \) and \( \kappa_2 = 1 \). The \( T_a \) statistics of five separate segments of signals each of time duration 5ms are averaged to improve the decision accuracy. The window sizes of \( \Psi \) and \( \Omega \) are chosen as five and ten, respectively.

Figure 7 displays the ROC curves of the detection method, for \( \beta = 2 \), under different values of SNR. It is clearly seen that increasing the SNR dramatically improves the detector performance. When the SNR is (or higher than) \(-21dB\), the detection rate exceeds 98% with the false alarm rate being 5%.

Figure 8 displays the ROC curves for SNR = \(-23dB\), under different values of \( \beta \). Even for such an extremely low SNR, the detection remains essentially error-free over a wide range...
Fig. 7. ROC curves of augmented SCF-based sensing method under different SNRs.

Fig. 8. ROC curves of augmented SCF-based sensing method under different $\beta$s.

of $\beta$s until $\beta$ gets as small as 2. On the other hand, in our simulation we observe a somewhat unexpected phenomenon that, if $\beta$ grows too large, say, several tens (not displayed in the figures herein), then the bandwidth dispersion in the wireless microphone signal becomes so severe that even the center peak in the PSD becomes diminished, making the denominator in $T_a$ small so as to decrease the value of $T_a$, and thus the detection rate drops.

V. EXPERIMENTAL VALIDATION

We present in this section experimental validation of the proposed sensing methods.

A. Experiment System Description

Figure 9 schematically illustrates the structure the experiment setup, and Figure 10 shows the experiment test bench. The experiment system consists of a wireless microphone, an antenna, a RF front-end module, and an oscilloscope. In experiments we use two makes of wireless microphones: one is Sennheiser EW100G2 which is capable of transmitting on 1440 frequency points (with a stepsize of 25kHz) between 786MHz and 822MHz, and the other is Shure UR8D which is capable of transmitting on 200 frequency points (with a stepsize of 160kHz) between 786MHz and 822MHz. The signals from a wireless microphone are received by the antenna, passed through the RF front-end module, and then fed to the oscilloscope where they are recorded and stored, before being processed by the computer program which implements the proposed sensing methods as described in the previous sections.

B. Experiment Results

We collected signal data using the wireless microphones indoors in a multi-floor building (Department of Electronic Engineering and Information Science in the west campus of University of Science and Technology of China), at a distance so as to sufficiently attenuate the received signal power. The wireless microphones were tested in both silent and voiced modes. In the silent mode there was no audio input to the wireless microphones, and in the voiced mode there was a recorded music playback to feed the wireless microphones at

1In China it has not been allowed to transmit on TV bands, so we choose to transmit on the spectrum just above the TV band upper edge, where the interference characteristics are quite similar as in TV bands.
Fig. 9. Schematic structure of sensing experiment setup.

moderate volume. For each make of wireless microphone in each mode, twenty experiments were conducted. Figures 11 and 12 are examples of the captured spectra of Sennheiser EW100G2 and Shure UR8D in silent mode, respectively, on a spectrum analyzer. Because the background noise power density in the spectrum analyzer was measured to be about $-139\text{dBm/Hz}$ (as indicated in the spectrum analyzer datasheet, and also can be confirmed from the figures taking into account the resolution bandwidth of $1.8\text{kHz}$), substantially higher than the ideal thermal noise density $-174\text{dBm/Hz}$, the wireless microphone signal power was set to roughly $-90\text{dBm}$, translating into a SNR approximately $-20\text{dB}$ over $8\text{MHz}$ TV channel bandwidth. Similar exercise was also conducted when recording wireless microphone signals in the oscilloscope.

In the experiments, we also tested the false alarm performance, by running the sensing methods for a number of noticeable narrowband interferences in the received spectrum. Every time such a narrowband interference being decided as a
wireless microphone signal, we interpreted it as a false alarm event.

1) Results of Periodogram-based Sensing Method: For Sennheiser EW100G2, in silent mode the detection rate $P_D$ was 100%, against the false alarm rate of $P_{FA} \approx 8%$; while in voiced mode, $P_D$ was 100% against $P_{FA} \approx 5%$. For Shure UR8D, in silent mode $P_D$ was 100% against $P_{FA} \approx 4%$; while in voiced mode, $P_D$ was 100% against $P_{FA} < 1%$. The trend in these results is consistent with the simulation in Section III-C.

2) Results of Augmented SCF-based Sensing Method: For each make of wireless microphone in each mode, $P_D$ was 100% without an occurrence of a false alarm event, throughout the twenty experiments. The augmented SCFs under different situations are displayed in Figure 13 for visual illustration. We clearly observe that, the shape of augmented SCF effectively captures the key difference between FM wireless microphones and CW-like narrowband interferences.

VI. CONCLUSION

We considered wireless microphone sensing in TVWS, treating its core problem of distinguishing between CW-like narrowband interference and FM wireless microphone signals. We developed two solutions, one based on periodogram and the other based on a proposed augmented SCF, to deal with this problem. Both the two solutions are logical consequences of our perceptual observations of the key features underlying CW and wireless microphone signals. Both simulation results and experimental validation results indicate that the proposed
solutions are promising for reliably sensing wireless microphones in TVWS.

There are a number of items in future work. First, for the proposed solutions, further analyzing their theoretical properties and computational complexities is important towards a full understanding of their potential and limitation. Second, for applying those solutions to real systems, hardware-oriented implementation techniques need to be studied and developed, and the developed experimental system needs to experience more extensive field tests, in order to fully validate the concepts.

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A. Statistical Properties of CW Periodogram and Frequency Offset Correction

With a frequency offset \( \Delta f = f_c - \hat{f}_c \), the down-converted baseband signal of CW can be written as

\[
x[n] = \frac{A}{2} e^{-j\varphi} e^{j2\pi n T_s} \Delta f + w[n].
\]  

For a length-\( N \) segment of \( x[n] \), after taking discrete Fourier transform (DFT), we obtain

\[
X[k] = \frac{1}{\sqrt{N}} \sum_{n=0}^{N-1} x[n] e^{-j2\pi kn/N} \]

\[
= \frac{A}{2\sqrt{N}} \sum_{n=0}^{N-1} e^{-j\varphi} e^{j2\pi n (\Delta f T_s - k/N)} + \frac{1}{\sqrt{N}} \sum_{n=0}^{N-1} w[n] e^{-j2\pi kn/N} \]

\[
= \frac{A}{2\sqrt{N}} e^{-j\varphi} e^{j\pi (N-1)\xi[k]} \text{sad}(\pi \xi[k], N) + \frac{1}{\sqrt{N}} \sum_{n=0}^{N-1} w[n] e^{-j2\pi kn/N} \]

\[
\triangleq X'[k] + W[k], \quad \text{for } k = 0, \ldots, N - 1,
\]

where \( \text{sad}(\pi \xi[k], N) \triangleq \frac{\sin(\pi N \xi[k])}{\sin(\pi \xi[k])} \) and \( \xi[k] \triangleq T_s \Delta f - k/N \). We also note that \( \text{sad}(0, N) = \lim_{\xi \rightarrow 0} \text{sad}(\pi \xi, N) = N \). The periodogram of \( x[n] \) is

\[
\xi[k] \triangleq |X'[k]|^2 = |X'[k]|^2 + X'[k] W^\dagger[k] + X'[\dagger k] W[k] + |W[k]|^2
\]

Due to the modeling assumption on noise, we have \( W[k] \sim \mathcal{CN}(0, \sigma^2) \), and consequently the mean and variance of \( \xi[k] \) are respectively

\[
\mathbb{E} \{ \xi[k] \} = \sigma^2 \left[ \frac{\text{SNR}}{N} \text{sad}^2(\pi \xi[k], N) + 1 \right]
\]

\[
\text{var} \{ \xi[k] \} = \sigma^4 \left[ \frac{2\text{SNR}}{N} \text{sad}^2(\pi \xi[k], N) + 1 \right].
\]

In order to suppress the effect of noise, we usually smooth out \( \xi[:i] \) by averaging \( M \) segments of such length-\( N \) periodograms to obtain an improve estimate of the PSD of the received signal, as \( \xi_a = (\xi_a[0], \xi_a[1], \ldots, \xi_a[N-1]) \) where the subscript \( a \) represents averaging over \( M \) segments.

Below is the procedure we used in our work to estimate the frequency offset \( \Delta f \). First, we identify the largest two elements in \( \xi_a \) as \( \xi_a[k_1] \) and \( \xi_a[k_2], k_1 < k_2 \), respectively. Then, by treating \( \xi_a[k] \) as the mean \( \mathbb{E} \{ \xi[k] \} \) in (18), we get

\[
\frac{\xi_a[k_1]}{\sigma^2} - 1 = \frac{\text{SNR}}{N} \text{sad}^2(\pi \xi[k_1], N)
\]

\[
\frac{\xi_a[k_2]}{\sigma^2} - 1 = \frac{\text{SNR}}{N} \text{sad}^2(\pi \xi[k_2], N).
\]
Taking their ratio leads to
\[
\left( \frac{\text{sad}(\pi\xi[k_1], N)}{\text{sad}(\pi\xi[k_2], N)} \right)^2 = \frac{\xi_a[k_1] - \sigma^2}{\xi_a[k_2] - \sigma^2}.
\] (22)

Now solving the equation (22) yields an estimate of $\Delta f$. We then correct the down-conversion frequency to $f_c + \Delta f$, which would be close to $f_c$, and perform the down-conversion procedure once again to come up with the hypothesis testing problem (23). Despite its simplicity, this correction procedure has shown satisfying performance in both simulation and experiments.

### B. The Detection Mechanism of Augmented SCF

For simplicity, we ignore the noise and write the signal vectors in the frequency domain of CW and FM wireless microphone signals as
\[
X[k] = \begin{cases} 
Ae^{j\xi k}, & k = 0 \\
0, & k = 1, \ldots, N - 1, and
\end{cases}
\] (23)
\[
X[k] = \begin{cases} 
A_k e^{j\xi_k}, & k \in [0, L - 1) \cup [N - L, N - 1], \\
0, & k \in [L, N - L - 1],
\end{cases}
\] (24)
respectively. Here $L$ denotes one half the size of nonzero frequency bins in the frequency domain. We pick the parameter $M$ in the definitions of SCF and conjugate SCF such that $L < \frac{M - 1}{2}$ holds.

For CW, the magnitudes of its augmented SCF can be explicitly evaluated as
\[
|\hat{S}^a_\alpha(f)_\alpha| = \begin{cases} 
\kappa_1 A^2_{\scriptscriptstyle MN}, & \alpha = 0, f \in [-\frac{M-1}{2N}, \frac{M-1}{2N}], \\
\kappa_2 A^2_{\scriptscriptstyle MN}, & \alpha = 0, f \not\in [-\frac{M-1}{2N}, \frac{M-1}{2N}].
\end{cases}
\] (25)

For FM wireless microphone signal, the situation is different since there are more than one nonzero frequency bins in the frequency domain. The magnitudes of its augmented SCF can be written as shown in the following.
\[
|\hat{S}^a_\alpha(f)_\alpha| = \begin{cases} 
\kappa_1 \frac{\sum_{k=-L}^{-N+L} A_k^2}{M N}, & \alpha = 0, f \in [-\frac{M-1}{2N}, \frac{M-1}{2N}], \\
\kappa_2 \frac{\sum_{k=-L}^{L} A_k^2}{M N}, & \alpha = 0, f \not\in [-\frac{M-1}{2N}, \frac{M-1}{2N}].
\end{cases}
\] (26)

Now for simplicity let us set $\Psi = [-\frac{2L}{N} + \frac{M-1}{N}, \frac{2L}{N} - \frac{M-1}{N}]$, and $\kappa_1 = \kappa_2 = 1$. In view of (25) for CW, we notice that the averaged magnitudes of its SCF (over $\alpha = 0$) and its conjugate SCF (over $f = 0$) are identical. In view of (26) for FM wireless microphone, however, its SCF (over $\alpha = 0$) and its conjugate SCF (over $\alpha = 0$) show different behaviors. That is, the magnitudes of the SCF (over $\alpha = 0$) within the window $\Psi$ are identically $\kappa_1 \frac{\sum_{k=-L}^{-N+L} A_k^2}{M N}$, while the magnitudes of the conjugate SCF (over $f = 0$) within the window $\Omega$ are $\kappa_2 \frac{\sum_{k=-L}^{L} A_k^2}{M N} e^{j(\xi_k - \xi_{-k})}$.

Due to the random phase incoherences $e^{j(\xi_k - \xi_{-k})}$ therein, empirically the conjugate SCF is expected to be much smaller than the SCF. In order to further enhance such a difference, in our detection method we adjust the weighting factors $\kappa_1$ and $\kappa_2$ to satisfy $\kappa_1 \ll \kappa_2$, so that the visual effect as shown in Figures 5 and 6 is clearly manifested.

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