A Possible Time-Delayed Brightening of the Sgr A* Accretion Flow after the Pericenter Passage of G2 Cloud

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Abstract

A possibility of time-delayed radio brightenings of Sgr A* triggered by the pericenter passage of the G2 cloud is studied by carrying out global three-dimensional magnetohydrodynamic simulations taking into account the radiative cooling of the tidal debris of the G2 cloud. Magnetic fields in the accretion flow are strongly perturbed and re-organized after the passage of G2. We have found that the magnetic energy in the accretion flow increases by a factor 3-4 in 5-10 years after the pericenter passage of G2 by a dynamo mechanism driven by the magneto-rotational instability. Since this B-field amplification enhances the synchrotron emission from the disk and the outflow, the radio and the infrared luminosity of Sgr A* is expected to increase around A.D. 2020. The time-delay of the radio brightening enables us to determine the rotation axis of the preexisting disk.

Key words: accretion, accretion disks — black hole physics — magnetohydrodynamics (MHD)

1 Introduction

The pericenter passage of an object named G2 close to the galactic center black hole (BH) Sgr A* (Gillessen et al. 2012) was expected to enhance the activity of Sgr A* by supplying the tidally stripped gas to the BH. The distance of its pericenter from the Galactic center BH is only \( \sim 2 \times 10^3 r_s \) (Gillessen et al. 2013a, 2013b), where \( r_s \) is the Schwarzschild radius. Br-\( \gamma \) observations indicate that the size of the G2 is \( \sim 15 \) mas, i.e., \( \sim 10^3 r_s \), which is as large as its pericenter distance. The estimated mass of the gas component of G2 is \( \sim 3 M_\odot \), which is comparable to that of the Sgr A* accretion flow, i.e., a hot accretion flow onto the Galactic center BH (for hot accretion flows, see Kato et al. 2008; Yuan & Narayan 2014, and references therein). The G2 was, therefore, expected to affect the dynamics of the Sgr A* accretion flow and trigger a flare. However, no brightening event induced by the pericenter approach of G2 has been observed in Sgr A* (Tsuboi et al. 2015; Bower et al. 2015).

After the discovery of the G2, a number of numerical simulations have been performed (Burkert et al. 2012; Schartmann et al. 2012; Sądowski et al. 2013; Abarca et al. 2014; Saitoh et al. 2014). Most of these simulations did not take into ac-
count magnetic fields despite their important roles in accretion processes (e.g., Balbus & Hawley 1991; Brandenburg et al. 1995; Matsumoto 1999; Hawley 2000; McKinney et al. 2012). Sadowski et al. (2013) carried out three-dimensional (3D) general relativistic magnetohydrodynamic (MHD) simulations in order to study the shock structure at which the electrons may be accelerated, during the pericenter passage of the G2 cloud. Long-term MHD simulations of the G2 cloud, however, have not yet been carried out, although it is necessary to explore the future brightening of Sgr A*.

In this paper, we present the possibility of the time-delayed amplification of magnetic fields and subsequent accretion by carrying out longer time-scale 3D MHD simulations of a hot accretion flow impacted by a cloud. Since the gas supplied by the cloud need a several rotation period at the pericenter to settle into a rotating torus, and typically 10 rotation period for the re-organization of magnetic fields, it takes 5-10 years until the magnetic fields are re-amplified by the dynamo action driven by the magneto-rotational instability (MRI). Therefore, in order to study the possibility of the time delayed brightening, we need to carry out MHD simulations for time scales of a decade. This is the motivation of this paper.

It is still controversial whether or not G2 harbors a star in its center: Pfuhl et al. (2015) observed G2 in infrared band using SINFONI and proposed that G2 is a pure gas clump, which is possibly formed from a gas stream around Sgr A*, while Witzel et al. (2014) observed G2 in L band using Keck observatory and proposed that G2 harbors a star because the size of the dust of G2 does not change during its pericenter passage. For simplicity, we assume pure gas clouds in this paper. This assumption should be reasonable, partly because a tidally disrupted gas feature is evident in $p$-$v$ diagram (Pfuhl et al. 2015), and partly because the size of the region where gravity of the central star dominates that of the Galactic center BH is only $\sim$1% of the estimated cloud size (Witzel et al. 2014), so that we can neglect the effect of the central star even if it exists.

### 2 Simulation Model

We solve a set of MHD equations taking into account the anomalous resistivity (Yokoyama & Shibata 1994) and the effects of radiative cooling in cylindrical coordinates ($\varpi$, $\varphi$, $z$). In this paper, $\varpi$ and $r$ denotes the cylindrical and the spherical radius, respectively. The equations are the same as those in Machida et al. (2006), except we incorporate the effects of radiative cooling due to recombination with approximate cooling function (Guillochon et al. 2014):

$$\Lambda_{\text{rec}} = 10^{-21} (\rho/m_p)^2 \exp[-(9/2)(\log T - 4)^2] \text{erg cm}^{-3} \text{s}^{-1},$$

as well as the bremsstrahlung emission $\Lambda_{\text{brem}} = 6.2 \times 10^{20} \rho^2 T^{1/2} \text{erg cm}^{-3} \text{s}^{-1}$, since the structure of the G2 cloud should be affected by the radiative cooling (Guillochon et al. 2014; Saitoh et al. 2014). Here, $m_p$, $\rho$, and $T$ is the proton mass, mass density, and gas temperature, respectively. In this work, we do not incorporate the effects of the synchrotron cooling. It is well known that, in optically-thin hot accretion disks, the bremsstrahlung cooling dominates the synchrotron cooling in the outer disk, which we simulate in this work, while the synchrotron cooling can be dominant in the inner disk. This is because the synchrotron cooling rate is roughly proportional to $T^4$ if we assume the energy equipartition, while the bremsstrahlung cooling rate is proportional to $T^{1/2}$. Since the gas temperature decreases with radius, the bremsstrahlung emission dominates the synchrotron radiation in the outer disks. In this work, as we mention below, we calculate the outer accretion flow, in which the bremsstrahlung emission is the dominant radiative process.

In addition, the G2 cloud is so cool that synchrotron emission cannot dominate the Br-\(\gamma\) and bremsstrahlung emissions, since the synchrotron photons are radiated by relativistic electrons. These are the reasons why we ignored the synchrotron cooling in this work. The anomalous resistivity is incorporated by using the same formula as that employed in Machida et al. (2006), i.e., $\eta = \eta_0 [(j/\rho)/(v_c - 1, 0)]^2$, where $\eta$ is the magnetic diffusivity, and $j$ is the current density. There are two free parameters: the coefficient for the anomalous resistivity $\eta_0$ and the threshold value $v_c$. We set $\eta_0 = 1.25 \times 10^{-3}$ and $v_c \sim 69.5$ in our simulation unit (i.e., $v_c = 0.9c$).

We carry out global 3D simulations by using a newly-developed MHD code CANS+ (Matsumoto et al. 2016). The code is based on the HLLD approximate Riemann solver proposed by Miyoshi & Kusano (2005). In order to preserve monotonicity and to achieve high-order accuracy in space, we employ a monotonicity preserving, fifth-order accurate interface value reconstruction method, MP5 (Suresh & Huynh 1997). A third-order TVD Runge-Kutta method is used for the time integration. We adopt the hyperbolic divergence cleaning method (Dedner et al. 2002) in order to minimize numerical errors of the divergence free condition of the magnetic field.

The number of computational cells is $(N_{\varpi}, N_{\varphi}, N_z) = (256, 128, 320)$. The cell size is constant in the inner region: $\Delta \varpi = \Delta z = 30r_s$ for $0 < \varpi < \varpi_0$ and $|z| < \varpi_0$. Here $\varpi_0$ is the location of the pressure maximum of the initial torus, which we set $\varpi_0 \equiv 3 \times 10^4 r_s$. Outside this region, $\Delta \varpi$ and $\Delta z$ increase with $\varpi$ and $z$, respectively: $\Delta \varpi_n = \min(1.05 \Delta \varpi_{n-1}, \Delta \varpi_{\max}), \Delta z_n = \min(1.05 \Delta z_{n-1}, \Delta z_{\max})$ for $z > 0$, and $\Delta \varpi_n = \min(1.05 \Delta \varpi_{n+1}, \Delta \varpi_{\max}), \Delta z_n$ for $z < 0$. Here, $n$ denotes the sequential cell number, and $\Delta \varpi_{\max}$ and $\Delta z_{\max}$ are set to be $200r_s$. In azimuthal direction, the cell size is set to be constant, i.e., $\Delta \varphi = (2\pi/N_{\varphi})$. The computational domain is, thus, $0 \leq \varpi \leq 4.323 \times 10^4 r_s$, $0 \leq \varphi \leq 2\pi$, and $|z| \leq 2.778 \times 10^4 r_s$. A spherical absorbing inner boundary is imposed at $r_{\text{in}} = 450r_s$, i.e., the physical quantity $q$ is approxi-
mated by \( q = q' - \epsilon' (q' - q_0) \) if their cell-centers are inside \( r_{in} \), where \( \epsilon' \) is the damping coefficient, \( q' \) is the numerically obtained quantity at the next timestep, and \( q_0 \) is the initial value [for details, see equation (7) and (8) in Machida et al. (2006)]. The shape of this absorbing boundary modestly matches up with the exact spherical one, since the cell size is \( \sim 5\% \) of the inner boundary radius. The outer boundaries are the free boundaries where waves can be transmitted.

At first, we perform the simulations of hot accretion flows without introducing a gas cloud until the accretion flow attains a quasi-steady state. After the quasi-steady state is realized, a gas cloud in pressure equilibrium with the ambient gas is located into the simulation box.

2.1 A Hot Accretion Flow Model for the Sgr A*

We assume a rotating, equilibrium torus with the pressure maximum at \( \pi = \pi_0 \). The torus is assumed to be threaded by a weak, purely toroidal, initial magnetic field, by using the equilibrium solution of magnetized tori proposed by Okada et al. (1989). The plasma \( \beta \) at the pressure maximum of the torus is initially 100. We set the direction of the rotation axis of the initial torus to be the same as \( z \)-axis. The torus is embedded in a hot, isothermal, non-rotating, static, coronal atmosphere with gas temperature \( \sim 1.3 \times 10^{10} \) K. For more details of the simulation set-up, see, e.g., Machida et al. (2006).

After the growth of the non-axisymmetric mode of MRI (\( \sim 10 \) orbital-period at the pressure maximum of the initial torus), the angular momentum is efficiently transported by the Maxwell stress and an accretion flow is formed. At 30 orbital-time at the pressure maximum, we locate a gas cloud in the computational domain to simulate the interaction of the G2 cloud with the Sgr A* accretion flow.

The normalization factor of the mass density \( \rho_0 \) is chosen to be consistent with the observational implication of mass density distribution of the Sgr A* accretion flow \( \rho_{\text{HIAF}}(r) = 1.3 \times 10^{-21} (r/10^4r_s)^{-1.125} \text{ g cm}^{-3} \) (Yuan et al. 2003; Anninos et al. 2012) such that \( \rho_0 \bar{\rho}(\pi_0) \approx \rho_{\text{HIAF}}(\pi_0) \), where \( \bar{\rho}(\pi_0) \sim 0.3 \) is the azimuthally averaged, normalized mass density of the quasi-steady accretion flow.

2.2 Models of the G2 Cloud

There are six parameters describing orbits of a point mass: the orbital inclination \( i \), the longitude of the ascending node \( \Omega \), the argument of the pericenter \( \omega \), the eccentricity \( e \), the semi-major axis \( a \), and the time of the pericenter passage \( t_0 \). The three parameters \( e, a, \) and \( t_0 \) can be constrained from the observations of the G2. According to the observation of the Br-\( \gamma \) emission line and the data analysis by Gillessen et al. (2013b), we set \( t_0 = A.D. \ 2014.25, \ e = 0.9762 \) and the pericenter radius \( r_p = a(1 - e) = 2.4 \times 10^3 r_s \). The semi-major axis \( a \) is obtained from \( e \) and \( r_p \). For convenience, we replace \( t - t_0 \) by \( t \) so that the G2 passes the pericenter at \( t = 0 \) yr.

For our simulations, the other three parameters \( i, \Omega, \) and \( \omega \) cannot be constrained from the observation, because of the uncertainty of the angle between the rotation axis of the Sgr A* accretion flow and that of the Galactic plane. For simplicity, we assume \( \Omega = 0 \) and \( \omega = 0 \), where \( \omega = 0 \) means that the pericenter is assumed to be on the equatorial plane of the accretion flows. We expect that the parameter \( \Omega \) does not significantly affect the results, because the global structure of the accretion flow is not highly non-axisymmetric. In this paper, we present results for \( t = 0 \) and \( \pi / 3 \) rad. In this work, we assume a Schwarzschild BH and employ a pseudo-Newtonian potential (Paczyński & Wiita 1980), so that we do not take into account the relation between the direction of the BH spin and the orbit parameters of the gas cloud described above.

We set the initial position of the center of G2 at \( r = 2.4 \times 10^3 r_s \). For the initial cloud density, we assume Gaussian distribution with FWHM = \( 3 \times 10^{15} \) cm (Sadowski et al. 2013) in such a way that the total mass of the gas cloud is \( 3M_\odot \). The initial velocity inside the cloud is assumed to be equal to the Kepler orbital velocity at its center of mass. For the sake of simplicity, we do not assume the initial magnetic field in the cloud. We note that \( \nabla \cdot B = 0 \) is assured when we locate the cloud, because the magnetic field is neither artificially added to nor removed from the computational domain.

The cloud which satisfy the assumption above is located in the computational domain after a quasi-steady accretion flow is formed.

3 Results

Time evolution of the gas cloud and the hot accretion flow when \( i = 0 \) is shown in figure 1. At \( t \simeq -4 \) yr (i.e., 30 Kepler orbital time at the initial pressure maximum of the torus), nonlinear growth of non-axisymmetric MRI has already been saturated, so that the accretion flow has attained the quasi-steady state. At this time, the spherical gas cloud is located at \( 2.4 \times 10^3 r_s \), far outside the zoomed region of figure 1. At \( t \simeq 0 \) yr, the gas cloud stretched by the tidal force of the Galactic center BH penetrates the accretion flow. This stage is qualitatively the same as Sadowski et al. (2013), except that the tidally stretched gas becomes slimmer due to the effects of the radiative cooling in this work. At \( t \simeq 5 \) yr, the accretion flow returns back to the quasi-steady state with its magnetic field being amplified by the MRI-driven-dynamo compared to that before the passage of the gas cloud. The mass density and pressure at \( r \gtrsim 3 \times 10^3 r_s \) is roughly half of those before the G2 encounter because the disk mass is swept by the G2 impact. However, the variation of mass density and gas pressure inside \( 2 \times 10^3 r_s \) (i.e., inside the pericenter radius of the G2 cloud) is about several tens per-
Snapshots of the simulated accretion flow before and after the passage of the gas cloud for the model with $i = 0$. Color maps show the mass density (top) and the magnetic energy density (bottom). The pericenter passage time estimated by using test particle approximation is defined as $t = 0$ yr. The dashed white curves represent the Kepler orbit of the center of G2.

In figure 2, we present time evolution of magnetic energy. The peak magnetic energy, which is 3-4 times larger than that before the encounter with G2, appears about 5 and 13 yrs after the pericenter passage of the G2 cloud for the model with inclination angle $i = 0$ and $\pi/3$, respectively. In the case that $i = 0$, magnetic energy decreases after the impact of the G2 cloud because the cloud collision increases the radial component of magnetic fields, which is subsequently amplified by differential rotation of the disk. In the case that $i = \pi/3$, magnetic energy slightly decreases after the cloud impact because the enhanced turbulent motion dissipates the magnetic energy. When the rotation axis of the disrupted disk is fixed, MRI-driven-dynamo

\begin{equation}
\rho_0 \approx 1.68 \times 10^{-20} \text{ g cm}^{-3} \quad \text{and} \quad v_0 \approx 3.87 \times 10^8 \text{ cm s}^{-1}
\end{equation}

are the initial torus mass density and the Keplerian velocity at $\tilde{r} = \tilde{r}_0 = 3 \times 10^3 r_s$, respectively.
amplifies the magnetic field of the tilted disk.

Here, let us discuss a little more about the competition between the magnetic dissipation and amplification. Since magnetic turbulence enhanced by the passage of the gas cloud increases the magnetic dissipation, the accretion flow approaches to a Taylor state (Taylor 1974), in which the system relaxes to a state with minimum magnetic energy. Figure 2 indicates that the relaxation of the magnetic energy is more significant in the model with $i = \pi / 3$, in which the system is highly perturbed by the impact of the cloud. Subsequently, magnetic field is amplified by MRI through the generation of $B_z$ by turbulence. Numerical results for $i = \pi / 3$ indicates that the magnetic field amplification by the latter mechanism becomes dominant 5 yrs after the pericenter passage of G2. This time scale is consistent with that of the disk dynamo at $\omega \sim 10^3 r_s$.

As mentioned above, the B-field amplification is delayed in the model with $i = \pi / 3$ because it takes time before the decay of strong perturbation caused by the impact of G2. Figure 3 shows time evolution of the angular momentum of the flows integrated such as $L = \int_{10r_s}^{750r_s} \int_{0}^{2\pi} \int_{-\pi/2}^{\pi/2} r \rho (r \times v) \varpi d\varpi d\varphi dz$. For the model with $i = \pi / 3$, the direction of the angular momentum is remarkably modified after the G2 passage: At $t \sim 0$ yr, the accretion flow is strongly disturbed by the cloud impact (see also figure 4) and the direction of angular momentum drastically changes. After $t \sim 5$ yr, the fluctuation of the $L_y$ and $L_z$ is less than $\sim 10\%$, so that it can be regarded that the flow has settled to a quasi-steady state with a tilted rotation axis. In this quasi-steady disk, the B-field amplification by MRI restarts to dominate the decay of the magnetic field. Thus, the amplification of the B-field in the model with $i = \pi / 3$ is delayed by 5 yrs.

In figure 4, it is shown that the accretion flow is tilted after the passage of the gas cloud for the model with $i = \pi / 3$. The tilt of the accretion flow is caused by the angular momentum transport from the gas cloud to the accretion flow, because the angular momentum of the accretion flow is misaligned with that of the initial orbital motion of the gas cloud. The angular momentum of the gas cloud is sufficient to change the direction of the angular momentum vector of the accretion flow. Since it requires several years for the rotation axis of the accretion flow to settle into the new direction, the B-field amplification via the disk dynamo is delayed when the inclination is large.

4 Summary and Discussion

We carried out 3D MHD simulations of the interactions of the Sgr A* accretion flow with the gas cloud G2, taking into account the effects of radiative cooling. We found that the magnetic energy increases by 3-4 times in 5-10 years after the pericenter passage of the G2 cloud. The delay time of the B-field amplification depends on the orbital inclination of the gas cloud: the maximum magnetic energy appears $\sim 5$ and $\sim 13$ yrs after the pericenter passage for the model with $i = 0$ and $\pi / 3$, respectively. The B-field amplification can increase the radio and the infrared luminosity with a time delay after the G2 passage.

We expect that the gradual increase of the synchrotron emission with a peak around A.D. 2020 can be observed in the radio and the infrared bands. This significant radio brightening should occur when the amplified magnetic field accretes to the innermost region. Furthermore, the X-ray flare may occur when the amplified magnetic energy is released via the magnetic reconnection in the vicinity of the BH.

Here, we discuss the consistency of our scenario with the no detection of the increased radiative flux in Sgr A* up to today. In this paper, we have found that the magnetic field in the Sgr A* accretion flow is amplified 5-10 yrs after the pericenter passage of the G2 cloud. Our scenario would reasonably explain the no detection of the radio and the infrared brightening to date, because the radio and the infrared emission in the Sgr A* may be dominated by the synchrotron emission, which should be enhanced with the B-field amplification.

By contrast, the X-ray emission of Sgr A* may be dominated by the bremsstrahlung emission from the outer part of the accretion flow at $\sim 10^3 r_s$ (Quataert 2002; Yuan et al. 2003). This radius is far outside the distance of the pericenter of G2. Thus, change of the dynamics of the inner accretion flow induced by the G2 impact will not affect the X-ray luminosity of Sgr A*, except the X-ray flare induced by the magnetic reconnection in the vicinity of the BH. It may be thought that the G2 should affect the X-ray luminosity when the cloud starts to interact with the accretion flow at $10^5 r_s$. However, since the size of G2 is only $\sim 10^3 r_s$, it would be too small to affect the dynamics of the accretion flow at $10^5 r_s$. No detection of increased X-ray emission up to today is, therefore, consistent with our scenario.
If the brightening is not detected during the next $\sim 10$ yrs, there can be two possible reasons: the location of the outer edge of the accretion flow is closer to the Galactic center BH than that of pericenter of th G2, or the gas component of G2 would be less massive than the expected one. The expectation for the brightening discussed above should be confirmed by calculating time-dependent multi-wavelength radiative spectra, by post-processing the MHD simulation data. In subsequent papers, we would like to carry out the spectral calculations, as well as the parameter survey of the MHD simulations of the disk-cloud interaction.

At the beginning of our simulations, the Br-\(\gamma\) luminosity obtained by volume integration of the cooling function expressed in equation (1) attains the luminosity $\sim 10^{-3}L_\odot$, which is consistent with the observed luminosity of the G2 (Gillessen et al. 2012). During the pericenter passage, however, the Br-\(\gamma\) luminosity decreases down to $\sim 10^{-4}L_\odot$ which is one order of magnitude lower than the observed one (Pfuhl et al. 2015). This inconsistency may be caused by overheating of the G2 cloud due to the numerical mixture of the G2 cloud and the hot accretion flows during the pericenter passage. This problem would be solved by performing the simulations with higher spatial resolution, as shown in simulations with adopted mesh refinement (AMR) code focusing not on the system including both the Sgr A* accretion flow and G2 cloud but on only G2 cloud (Schartmann et al. 2015). However, the B-field amplification shown in this work should occur also in simulations with fine spatial resolution, since it is driven by the disk dynamo (especially by MRI) and the high-resolution-simulations rather show more efficient B-field amplification (Hotta et al. 2016). Simulations with higher spatial resolution reproducing the consistent luminosity of the Br-\(\gamma\) emission remains as a future work.

It should be noted that, after the pericenter passage of the G2 cloud, the mass accretion rate at the inner boundary ($450r_s$) increases 2-4 times of that before the G2 impact in our simulations. However, since the magnetic energy inside the disk does not increase until the MRI driven dynamo grows again (i.e., 5-10 years after the G2 impact), the synchrotron luminosity would not increase significantly until the strongly magnetized region begins to infall.

When the gas with the amplified B-fields accrete onto the inner disk, synchrotron emission from the inner disk will increase. Although the observational images would not be perfectly the same as those predicted by Mo\'scibrodzka et al. (2012) because of the amplification of the magnetic field after the G2 encounter in our study, synchrotron brightened region may be similar to that studied by Mo\'scibrodzka et al. (2012). The brightening may be detected by East Asia mm/submm VLBI observation and Event Horizon Telescope submillimeter Very Long Baseline Interferometry experiment (EHT). As discussed below, the angle between the rotation axis of the accretion disk
and the orbital axis of the G2 may be constrained by these observations.

Let us discuss whether or not the direction of the rotation axis of the preexisting accretion flow can be constrained by the timing of the brightening. The radio brightening in the vicinity of the BH is expected to follow the amplification of the B-field at $\sim 10^{3}r_{s}$, i.e., the increased B-field will be advected inward and, subsequently, will be amplified further near the BH. If we assume that the amplified B-field is advected to the innermost region of the accretion flow in the viscous accretion timescale, the time lag due to the advection is $\lesssim 1$ yr, where we have assumed viscosity parameter (Shakura & Sunyaev 1973) $\alpha \approx 0.1$ since our simulations indicate this value in the B-filed re-amplification stage. This accretion timescale is shorter than the timescale of the B-field amplification $\sim 5$ or $\sim 10$ yrs so that we can identify the difference of the orbital inclination of G2 against the preexisting accretion flow. The comparison of the timing of brightening in the simulation with the future observation would enable us to constrain the direction of the rotation axis of the preexisting Sgr A* accretion flow, since the orbital plane of the G2 is known. Furthermore, the tilt of the accretion flow in $i = \pi/3$ case (figure 4), can be spatially resolved by the East Asia mm/submm VLBI observation and EHT. If the direction of the rotation axis of the accretion disk significantly differs from the angular momentum axis of G2, we would be able to observe the change of the rotation axis of the accretion flow with time.

The tilt of the accretion flows caused by the disk-cloud interaction may occur not only in Sgr A* but also in the other low luminosity active galactic nuclei (LLAGNs). The tilt may induce the quasi-periodic oscillation in the LLAGNs and/or the change of the direction of the LLAGN jets. These possible behaviors would be important to explore the accretion and ejection histories in LLAGNs.

In this work, we set the inclination $i = 0$ and $\pi/3$, i.e., the gas cloud is assumed to be co-rotating with the accretion disk. If the gas cloud is counter-rotating with the accretion disk, we expect that the retrograde gas cloud will lose more angular momentum than the prograde one does affected because of the ram pressure of the accretion flow. Especially in the perfectly retrograde case (i.e., $i = \pi$), the most part of gas cloud may not be able to keep the Keplerian orbit, which is estimated by the observations of Br-γ emission line, until the G2 reaches the pericenter. It may also excite a strong disturbance of the accretion flow due to the mixing of the gas with opposite angular momentum, which would result in the drastic increase of mass accretion rate onto the black hole. We leave the parameter study of the gas cloud including the counter-rotating case as a future work.

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