Quantifying the effects of long-range $^{13}$C-$^{13}$C dipolar coupling on measured relaxation rates in RNA

Lukasz T. Olsenginski$^1$ · Theodore K. Dayie$^1$

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Abstract
Selective stable isotope labeling has transformed structural and dynamics analysis of RNA by NMR spectroscopy. These methods can remove $^{13}$C-$^{13}$C dipolar couplings that complicate $^{13}$C relaxation analyses. While these phenomena are well documented for sites with adjacent $^{13}$C nuclei (e.g. ribose C1′), less is known about so-called isolated sites (e.g. adenosine C2). To investigate and quantify the effects of long-range (> 2 Å) $^{13}$C-$^{13}$C dipolar interactions on RNA dynamics, we simulated adenosine C2 relaxation rates in uniformly [U-$^{13}$C/$^{15}$N]-ATP or selectively [2-$^{13}$C]-ATP labeled RNAs. Our simulations predict non-negligible $^{13}$C-$^{13}$C dipolar contributions from adenosine C4, C5, and C6 to C2 longitudinal (R$_1$) relaxation rates in [U-$^{13}$C/$^{15}$N]-ATP labeled RNAs. Moreover, these contributions increase at higher magnetic fields and molecular weights to introduce discrepancies that exceed 50%. This will become increasingly important at GHz fields. Experimental R$_1$ measurements in the 61 nucleotide human hepatitis B virus encapsidation signal ε RNA labeled with [U-$^{13}$C/$^{15}$N]-ATP or [2-$^{13}$C]-ATP corroborate these simulations. Thus, in the absence of selectively labeled samples, long-range $^{13}$C-$^{13}$C dipolar contributions must be explicitly taken into account when interpreting adenosine C2 R$_1$ rates in terms of motional models for large RNAs.

Keywords Dipolar coupling · Relaxation · Dynamics · NMR spectroscopy · Nucleic acids

Introduction
RNAs are important macromolecules that function in a wide range of cellular roles (Cech and Steitz 2014; Mortimer et al. 2014; Sharp 2009). Despite being composed of only four ribonucleotide building blocks, RNAs are capable of adopting complex three-dimensional structures that impart functionality (Dethoff et al. 2012; Ganser et al. 2019). Moreover, RNAs are dynamic and can sample numerous conformations on various time scales that might be important for function (Zhao et al. 2017; Marušič et al. 2019). Solution nuclear magnetic resonance (NMR) spectroscopy is a high-resolution biophysical technique that is well suited to probe these dynamic RNA structures. Three commonly measured dynamics parameters are the longitudinal (R$_1$) and transverse (R$_2$) relaxation rates and the heteronuclear Overhauser effect (hNOE) (Marušič et al. 2019; Palmer 2004; Wagner 1993).

The R$_1$ rate measures the return of the longitudinal magnetization to thermal equilibrium whereas R$_2$ measures the decay of transverse magnetization, and the hNOE measures the change in heteronuclear spin magnetization in response to saturating proton spins (Yamazaki et al. 1994; Peng and Wagner 1992; Abragam 1961).

RNA motions directly influence these R$_1$, R$_2$, and hNOE relaxation parameters (Marušič et al. 2019; Palmer 2004; Wagner 1993; Yamazaki et al. 1994; Peng and Wagner 1992; Abragam 1961; Spiess 1978; Hansen and Al-Hashimi 2007; Nirmala and Wagner 1988; Palmer et al. 1991). Depending on the probed nuclei, dipolar interactions and chemical shielding anisotropy (CSA) mechanisms contribute predominantly to R$_1$ and R$_2$ relaxation, and dipolar interactions to the hNOE. These three relaxation measurements can be fit to extract motional variables such as overall correlation time ($\tau_C$) and the square of the generalized order parameter ($S^2$) that describe fast (ps-ns) dynamics in RNA within a Model Free formalism (Spiess 1978; Lipari and Szabo 1982) or combined Model Free and reduced spectral density mapping implemented in ROTDIF (Berlin et al. 2013). Therefore, accurate R$_1$, R$_2$, and hNOE measurements are crucial for
obtaining precise dynamics information and drawing valid conclusions about RNA molecular recognition events.

These dynamic RNA motions are most often measured by using $^{13}$C (Boisbouvier et al. 1999; Dayie et al. 2002) and $^{15}$N (Dayie et al. 2002; Akke et al. 1997) nuclei as indirect probes. However, imino and amino $^{15}$N nuclei experience solvent exchange and are only visible in structured regions, making non-protonated $^{15}$N (e.g. purine N7) and protonated $^{13}$C (e.g. adenosine C2) nuclei attractive probes. The latter sites are present in both the nucleobase and ribose moieties and therefore provide more coverage of RNA structure. Still, large $^{13}$C-$^{13}$C scalar and dipolar couplings in uniformly $^{13}$C/$^{15}$N labeled RNA can complicate analyses of these sites (Yamazaki et al. 1994; Kay et al. 1989; Alvarado 2014; Johnson et al. 2006; Thakur and Dayie 2012; Nam et al. 2020; Thakur et al. 2012). Indeed, the effect of dipolar couplings on RNA relaxation has been studied for sites with adjacent $^{13}$C nuclei (e.g. ribose C1’). These investigations demonstrate that dipolar interactions from attached $^{13}$C atom(s) lead to deviations from monoexponential decay and discrepancies in the extracted $R_1$ rate for ribose C1’ (Alvarado 2014; Thakur and Dayie 2012; Nam et al. 2020; Thakur et al. 2012), C2’ and C4’ (Johnson et al. 2006), as well as for pyrimidine C6 (Nam et al. 2020; Thakur et al. 2012). However, much less is known about isolated sites such as purine C8 or adenosine C2. We recently showed that purine C8 may experience non-negligible dipolar contributions to $R_1$ relaxation from non-adjacent coupling partners (Nam et al. 2020). The extent to which adenosine H2-C2 approximates an isolated spin pair remains unclear.

To investigate and quantify the effects of long-range (> 2 Å) $^{13}$C-$^{13}$C dipolar coupling on RNA dynamics, we simulated adenosine C2 relaxation rates in uniformly [U-$^{13}$C/$^{15}$N]-ATP or selectively [2-$^{13}$C]-ATP labeled RNAs. Our simulations predict non-negligible $^{13}$C-$^{13}$C dipolar contributions from adenosine C4, C5, and C6 to $R_2$ rates in [U-$^{13}$C/$^{15}$N]-ATP labeled RNAs that increase with higher magnetic fields and molecular weights. To empirically test our simulations, we measured adenosine C2 relaxation in the 61 nucleotide (nt) human hepatitis B virus encapsidation signal ε (HBV ε) RNA (Flodell et al. 2006; Lee 1997; Knaus and Nossal 1993; Hirsch et al. 1990) labeled with [U-$^{13}$C/$^{15}$N]-ATP or [2-$^{13}$C]-ATP. To this end, we used our recently synthesized [2-$^{13}$C, 7-$^{15}$N]-ATP (Olenginski and Dayie 2020) as a selective adenosine $^{13}$C2 labeled probe. We demonstrate that the removal of long-range $^{13}$C-$^{13}$C dipolar coupling partners reveals discrepancies in measured adenosine C2 $R_1$ values between uniformly and selectively labeled samples. Moreover, $R_1$ measurements at lower temperature (mimicking increased molecular weight) revealed exacerbated $R_1$, $R_2$ discrepancies, which further corroborates our simulations and argues that selective $^{13}$C2 labeled probes obviates the need to account for the significant contributions to measured $R_{1,2}$ that arise from neighboring $^{13}$C atom(s) in RNAs with a $\tau_c$ > 20 ns. Our [2-$^{13}$C, 7-$^{15}$N]-ATP (Olenginski and Dayie 2020) also showed better spectroscopic properties than [U-$^{13}$C/$^{15}$N]-ATP, providing and additional advantage to using selectively labeled samples to measure RNA dynamics.

**Materials and methods**

**Theoretical simulations**

$^{13}$C $R_1$ and $R_2$ relaxation rates and steady-state $^{13}$C{$^1$H} hNOE values were simulated using Eqs. 1–6, (Palmer 2004; Peng and Wagner 1992; Abragam 1961). We assumed isotropic tumbling. These relaxation parameters were simulated for adenosine C2 in [U-$^{13}$C/$^{15}$N]-ATP or [2-$^{13}$C]-ATP labeled RNAs and included dipolar contributions from adenosine C4, C5, C6, N1, and N3 at average distances of 2.20, 2.70, 2.30, 1.40, and 1.30 Å, respectively. In addition, adenosine C2 experiences dipolar contributions with the following protons: (1) the attached H2, (2) those within the same nucleotide, (3) those 3’-same strand, and (4) those 3’-cross-strand contacts (Wijmenga and Buuren 1998). Protons in (2) are H1’ and H2’ at average distances of 4.35 and 4.20 Å. Protons in (3) are H1, H2, amino (N)H$_2$, and H1’ at average distances of 4.00, 4.40, 4.33, and 4.45 Å. Protons in (4) are H1, H3, amino (N)H$_2$, and H1’ at average distances of 4.10, 4.50, 4.40, and 4.95 Å. All proton distances above were calculated from pdb 2ixy (Flodell et al. 2006) as a representative A-helical RNA. Solution NMR derived CSA values ($\sigma_{11}=89$, $\sigma_{22}=15$, $\sigma_{33}=-104$) (Ying et al. 2006) and an aromatic CH bond length of 1.104 Å (Fiala et al. 2000) were used in these simulations.

**RNA sample preparation**

In vitro transcriptions of RNA were performed as previously described (Milligan and Uhlenbeck 1989). In brief, transcriptions were carried out in 40 mM Tris–HCl pH 8 (at 37 °C), 1 mM spermidine, 0.01% Triton X-100, 80 mg/ml PEG, 0.3 μM DNA template, 1 mM 1,4-dithiothreitol, 2 U/μl thermostable inorganic pyrophosphatase, 5–20 mM rNTPs, 5–20 mM MgCl$_2$, and 0.1 mg/mL T7 RNA polymerase. Reactions proceeded for 3 h at 37 °C. For each RNA transcribed, the concentrations of MgCl$_2$ and rNTPs were optimized. DNA template and [U-$^{13}$C/$^{15}$N]-ATP were purchased from Integrated DNA Technologies and Cambridge Isotope Laboratories, respectively. The [2-$^{13}$C, 7-$^{15}$N]-ATP was synthesized as recently described (Olenginski and Dayie 2020). After transcription, samples were extracted with acid-phenol:chloroform, ethanol precipitated, purified by preparative denaturing gel
electrophoresis, and electroeluted. The samples were subsequently dialyzed five times against UltraPure ddH2O, folded in NMR buffer (10 mM Na3PO4 pH 6.5, 0.1 mM EDTA), lyophilized, and resuspended in 100% D2O. NMR samples of HBV ε labeled with [U-13C/15N]-ATP or [2-13C, 7-15N]-ATP had a final concentration of 0.35 mM in 0.30 ml (calculated using a molar extinction coefficient of 768.3 mM−1 cm−1).

NMR spectroscopy

All NMR experiments were performed on an 800 MHz Avance III Bruker spectrometer equipped with a triple resonance cryogenic probe. NMR relaxation data were collected at either 5 or 25 °C as specified in the text and figure legends. TROSY-detected measurements of 13C R1 and R1ρ relaxation rates and steady-state 13C[1H] hNOE values were adapted from previous pulse sequences (Hansen and Al-Hashimi 2007; Lakomek et al. 2013). For R1 experiments at 25 °C, relaxation delays of 0.10, 0.20 (× 2), 0.36, 0.50, 0.90, and 1.20 s (with both [U-13C/15N]-ATP and [2-13C, 7-15N]-ATP labeled sample) were used. For R1 experiments at 5 °C, relaxation delays of 0.10, 0.20 (× 2), 0.80, 1.00, 1.20 (with [U-13C/15N]-ATP labeled sample) or 0.10, 0.20 (× 2), 0.90, 1.10, 1.30 (with [2-13C, 7-15N]-ATP labeled sample) were used. For R1p experiments, relaxation delays of 1.5, 2.4, 3.4, 4.6, 6.1, 8.0, and 11.0 ms (at 25 °C) or 1.0, 2.0, 4.0, 5.0, and 6.0 ms (at 5 °C) were used and the strength of the spin-lock field (ω1) was 1.9 kHz. R1 and R1p experiments were acquired in an interleaved manner as a pseudo-three-dimensional experiment and using a recycle delay of 2.5 s. For 13C[1H] hNOE (saturation) experiments, recycle and saturation delays of 1.5 and 7 s were used and proton saturation was achieved using a train of hard 180° pulses. In the 13C[1H] hNOE (no saturation) experiments, a delay of 8.5 s was used in order to match the time of both recycle and saturation delays from the saturation experiment. For experiments on [U-13C/15N]-ATP labeled HBV ε, selective pulses were applied as previously described (Hansen and Al-Hashimi 2007; Nam et al. 2020). Shape pulses used for on-resonance 13C inversion, on-resonance 13C refocusing, and off-resonance 13C inversion were Q3 (Emsley and Bodenhausen 1992), RSNOB (Kupče et al. 1995), and IBURP2 (Geen and Freeman 1991), respectively. Q3 pulse selectively inverts the 13C magnetization of interest, whereas RSNOB and IBURP2 selectively refocus (invert) 13C magnetization to eliminate 13C-13C scalar coupling evolution. Pulse lengths for each pulse were 937.5, 1000, and 450 μs, respectively. The offset and bandwidth for IBURP2 were ± 40 and 50 ppm, respectively. 15N was decoupled.

Data analysis

NMR spectra were processed and analyzed using TopSpin 4.0, NMRFx Processor, and NMRViewJ (Norris et al. 2016; Johnson and Blevins 1994). R1 and R1ρ relaxation rates were determined by fitting peak intensities to a monoexponential decay. Uncertainties in R1 rates were estimated by propagating the error in peak intensities from duplicated delay points (indicated by “×2” above). R2 rates were corrected for the off-resonance ω0 using Eqs. 7 and 8. Uncertainties in R1p rates were determined by the RELAXFIT (Fushman et al. 1997) Matlab program. The steady-state 13C[1H] hNOE was obtained using (1 + η) (Peng and Wagner 1992; Palmer et al. 1991; Clore et al. 1990a, b; Weaver et al. 1988). Uncertainties in 13C[1H] hNOE values were estimated by propagating the error in peak intensities in duplicated experiments.

Results and discussion

Effects of long-range dipolar couplings on adenosine C2 relaxation

Before quantifying the effects of dipolar couplings on RNA dynamics, it is informative to consider the various relaxation contributions to our targeted nuclei. The 13C R1 and R2 rates of adenosine C2 (R1,C2 and R2,C2) are given by

$$R_{1,C2} = \sum_i R_{1,C2,H_i} + \sum_j R_{1,C2,C_j} + \sum_k R_{1,C2,N_k} + R_{1,CSA}$$  \hspace{1cm} (1)

$$R_{2,C2} = \sum_i R_{2,C2,H_i} + \sum_j R_{2,C2,C_j} + \sum_k R_{2,C2,N_k} + R_{2,CSA} + R_{cs}$$  \hspace{1cm} (2)

wherein the auto R1,C2 (R(C,C)) and R2,C2 (R(C,C)) rates and cross-relaxation (R(C → C)) functions of the underlying spectral density function (Palmer 2004; Peng and Wagner 1992; Abragam 1961):

$$R_{1,C2} = R_c(C,C) = \frac{1}{4} D_{C,C}\frac{2}{2}J(\omega_i - \omega_C) + 3J(\omega_C) + 6J(\omega_C + \omega_i) + C_i^2/J(\omega_C)$$  \hspace{1cm} (3)

$$R_c(H^C → C) = \frac{1}{4} D_{C,i}^2 [6J(\omega_C + \omega_i) - J(\omega_i - \omega_C)]$$  \hspace{1cm} (4)

$$R_{2,C2} = R_c(C,C) = \frac{1}{8} D_{C,i}^2 [4J(0) + J(\omega_i - \omega_C) + 3J(\omega_C) + 6J(\omega_i) + 6J(\omega_C + \omega_i) + C_i^2 4J(0) + 3J(\omega_C)]$$  \hspace{1cm} (5)
\( R_{1,C} \) is the dipolar chemical exchange contribution to \( R_2 \), \( D_{1,C} \), and \( C_C \) are the dipolar coupling (\( \mu_0 \gamma_i^2 \mu / 4 \pi r^3 \)) and CSA (\( \alpha_i \Delta \sigma_{ij} / \sqrt{3} \)) constants, respectively, where \( \gamma_i \) is the gyromagnetic ratio of spin \( i \) (where \( i \) can be \( \text{H}, \text{C} \), or \( \text{N} \)), \( r \) is the distance between the two spins, \( \mu_0 \) is the permeability of free space, \( h \) is Plank’s constant divided by 2\( \pi \), and

\[
\Delta \sigma_{ij} = \left( \frac{1}{\gamma_1^2} + \frac{1}{\gamma_2^2} - \frac{1}{\gamma_{12}^2} \right) \sigma_{ij}. \quad \text{Here, } \sigma_{ij} = \sigma_{zz} - \sigma_{ij}, \\
\sigma_{zz} = \sigma_{33} - \sigma_{22} + \sigma_{11}, \quad \sigma_{11} = \sigma_{33} - \sigma_{22}, \quad \text{and } \sigma_{33} \text{ are the principal components of the chemical shielding tensor (Ying et al. 2006; Fushman et al. 1998) and } J(\omega) \text{ is the spectral density function assuming isotropic tumbling. The auto- and cross-relaxation rates combine to give the steady-state } ^{13}\text{C}\{^1\text{H}\} \text{ hNOE (} \eta \text{) (Peng and Wagner 1992; Palmer et al. 1991; Clore et al. 1990a, b; Weaver et al. 1988)}
\]

\[
\eta = \left( \frac{I_{sat}}{I_{eq}} \right) = \frac{\gamma_R C(H_z^C \to C_z)}{\gamma_R H_{1,C2}},
\]

where \( I_{sat} \) and \( I_{eq} \) are signal intensities of the \( ^{13}\text{C} \) resonances when the \( ^{1}\text{H} \) resonances are saturated or not.

As seen in Eqs. 1–5, adenosine \( R_{1,C2} \) and \( R_{2,C2} \) rates incorporate dipolar interactions with nearby \( ^{1}\text{H}, \text{C} \), and \( ^{15}\text{N} \) nuclei, as well as the \( ^{13}\text{C} \) CSA. For small-to-medium sized RNAs with a \( \tau_c < 10 \text{ ns} \), \( ^{1}\text{H}-^{13}\text{C} \) dipolar and \( ^{13}\text{C} \) CSA contributions dominate adenosine \( R_{1,C2} \) and \( R_{2,C2} \) relaxation. At 800 MHz, the \( ^{13}\text{C} \) dipolar and \( ^{13}\text{C} \) CSA contribution to adenosine \( R_{1,C2} \) is 43–71% and 29–52%, respectively, whereas their contribution to adenosine \( R_{2,C2} \) is 43–64% and 36–57%, respectively \( ^{13}\text{C} \) CSA and dipolar contributions are defined as \( [100 \times (^{13}\text{C}\text{CSA/}^{13}\text{C}\text{Dipolar})] \) and \( [100 \times (^{13}\text{C}\text{Dipolar/}^{13}\text{C}\text{Dipolar})] \). Where \( \text{CSA} \) and dipolar terms are those found in Eqs. 3 and 5 (Supplementary Fig. S1a and b). Therefore, for these RNAs, the dipolar contributions from surrounding \( ^{13}\text{C} \) (< 4%) and \( ^{15}\text{N} \) (< 1%) nuclei are negligible and can likely be ignored. However, \( ^{13}\text{C} ^{13}\text{C} \) dipolar interactions contain an additional \( J(0) \) term arising from \( J(\omega_{c2} - \omega_{c1}) \), which increases as a function of \( \tau_c \) and magnetic field strength. Moreover, the bonafide \( J(0) \) term in \( R_{2,C2} \) is pre-multiplied by 4 and is linked with the direct H2-C2 dipolar vector that is larger than any \( ^{13}\text{C} ^{13}\text{C} \) dipolar vector by ~16 due to the contribution from the gyromagnetic ratios alone. Taken together, \( ^{13}\text{C} ^{13}\text{C} \) dipolar interactions are expected to negligibly contribute to adenosine \( R_{2,C2} \) (< 0.1%) and significantly contribute to \( R_{1,C2} \) as RNAs increase in size and higher magnetic fields are used. Indeed, at 800 MHz, these \( ^{13}\text{C} ^{13}\text{C} \) dipolar contributions to adenosine \( R_{1,C2} \) rise to 20, 50, and 80% in larger RNAs with a \( \tau_c \) of 25, 50, and 100 ns (Supplementary Figs. S1c and d). Moreover, these contributions further increase at higher magnetic fields (Supplementary Figs. S1c and d).

In \([\text{U-}^{13}\text{C}/^{15}\text{N}]\text{-ATP} \) labeled RNAs, adenosine \( C2 \) is dipolar coupled to the attached H2, the adjacent N1 and N3, and the long-range (> 2 Å) C4, C5, and C6 atoms (Fig. 1a, inset). Moreover, in fully protonated RNA, adenosine \( C2 \) also experiences long-range dipolar contributions from protons within the same nucleotide, those 3’ and on the same strand, and those 3’ and on the cross-strand (Wijmenga and Buuren 1998). If these long-range dipolar couplings contribute significantly to RNA relaxation, theoretical simulations should reveal discrepancies in adenosine \( R_{1,C2} \) and \( R_{2,C2} \) rates and steady-state \( ^{13}\text{C}\{^1\text{H}\} \text{ hNOE values in } [\text{U-}^{13}\text{C}/^{15}\text{N}]\text{-ATP} \) and [\( ^{2}\text{C}\text{-ATP} \) labeled RNAs. To test this hypothesis, we used previously reported CSA values derived from solution NMR (Ying et al. 2006) and Eqs. 1–6, (Palmer 2004; Peng and Wagner 1992; Abramag 1961) to simulate adenosine \( R_{1,C2} \) and \( R_{2,C2} \) relaxation rates and steady-state \( ^{13}\text{C}\{^1\text{H}\} \text{ hNOE}

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\( \text{Fig. 1} \) Adenosine \( R_{1,C2} \) simulations in \([\text{U-}^{13}\text{C}/^{15}\text{N}]\text{-ATP} \) or \([^{2}\text{C}\text{-ATP} \) labeled RNAs. a) Simulated adenosine \( R_{1,C2} \) rates with a scheme of adenine (numbered by atom and with interatomic distances (Å) to \( C2 \) shown as an inset. b) Simulated adenosine \( R_{1,C2} \) percent difference (diff.) \( [100 \times (^{13}\text{C}^{12}\text{C}^{\text{uniform}}/^{13}\text{C}^{12}\text{C}^{\text{selective}})^{13}\text{C}^{12}\text{C}^{\text{uniform}}] \). c) Simulated adenosine \( R_{1,C2} \) percent difference for each dipolar coupling partner (C4, C5, C6, N1, and N3). All simulations assume isotropic tumbling and those in b were carried out with increasing magnetic field strengths and overall correlation times (\( \tau_c \)) whereas those in a and c are at 800 MHz. Solution NMR derived CSA values \( (\sigma_{12} = 15, \sigma_{22} = 104) \) (Ying et al. 2006) and an aromatic CH bond length of 1.104 Å (Fiala et al. 2000) were used. Our simulations suggest that dipolar interactions result in underestimated \( R_{1,C2}^{\text{uniform}} \) rates that increase with higher magnetic fields and molecular weights.
values in [U-13C/15N]-ATP or [2-13C]-ATP labeled RNAs (see “Materials and Methods” section). For simplicity, our simulations assume isotropic tumbling as the effects of long-range dipolar couplings are more readily quantifiable.

We do not observe differences in the simulated $R_{2,C2}$ rates or steady-state $^1C\langle^1H\rangle$ hNOE values (Supplementary Fig. S2), in agreement with previous studies (Yamazaki et al. 1994; Hansen and Al-Hashimi 2007; Nam et al. 2020). However, our simulations do predict discrepancies in $R_{1,C2}$ rates (Fig. 1a) between uniformly and selectively labeled samples ($R_{1,C2\text{(uniform)}}$ and $R_{1,C2\text{(selective)}}$, respectively), an observation similar to that recently reported for purine C8 sites (Nam et al. 2020). Specifically, dipolar interactions result in overestimated $R_{1,C2\text{(uniform)}}$ rates that increase with higher magnetic fields and molecular weights (Fig. 1a), as predicted by Eq. 3 (Supplementary Fig. S1a). Moreover, the percent difference in $R_{1,C2}$ (defined as \(\frac{100\% (R_{1,C2\text{(uniform)}} - R_{1,C2\text{(selective)}})}{R_{1,C2\text{(uniform)}}}\)) is predicted to be at least 80% at 1.2 GHz and a $\tau_c$ of 100 ns (Fig. 1b). While RNAs of this size are rarely probed by NMR, the simulated discrepancies are still significant for smaller RNAs. As highlighted by our simulations, $^{13}C\cdot^{13}C$ dipolar interactions dominate the discrepancy whereas $N1$ and $N3$ have almost no effect. Moreover, the $^{13}C\cdot^{13}C$ contributions scale with atomic distance from C2, with C4 (2.2 Å) having the greatest effect followed by C6 (2.3 Å) and then C5 (2.7 Å) (Figs. 1a, inset and c).

Adenosine C2 $R_1$ measurements in uniformly and selectively labeled RNA

Our newly synthesized [2-13C, 7-15N]-ATP (Olenginski and Dayie 2020) removes unwanted $^{13}C\cdot^{13}C$ and $^{13}C\cdot^{15}N$ dipolar interactions and was therefore used along with commercially available [U-13C/15N]-ATP to empirically test our simulations. To this end, we measured adenosine $R_{1,C2}$ rates for [U-13C/15N]-ATP or [2-13C, 7-15N]-ATP labeled HBV $\varepsilon$ (Fig. 2) at 800 MHz and 25 °C using TROSY-detected pulse sequences (Hansen and Al-Hashimi 2007; Lakomek et al. 2013; Weigelt 1998; Pervushin et al. 1997). In agreement with our simulations (Fig. 1a), $R_{1,C2\text{(uniform)}}$ was significantly higher than $R_{1,C2\text{(selective)}}$ for 6 of the 8 HBV $\varepsilon$ adenosine residues (Fig. 3a). Explanations for why A29 and A55, in particular, differ from the other residues requires detailed structural information which is currently lacking. Nevertheless, our simulated and experimental trends show good agreement on the whole. That is, the average percent difference in measured $R_{1,C2}$ rates was 4.7% (Fig. 3b) compared to the simulated 5.4% (Fig. 2b) for an RNA with a $\tau_c$ of 11 ± 1 ns at 800 MHz (measured from $R_2/R_1$ (Fushman et al. 1994; Thakur et al. 2010)) (Supplementary Fig. S3). While this discrepancy is small and can likely be ignored, our simulations suggest that this is no longer true as RNAs increase in size.

To experimentally verify that the discrepancy in $R_{1,C2}$ increases at higher molecular weights, we repeated our $R_{1,C2}$ measurements in [U-13C/15N]-ATP or [2-13C, 7-15N]-ATP labeled HBV $\varepsilon$ at 5 °C to simulate an RNA with a higher molecular weight (larger $\tau_c$). To maximize signal-to-noise and minimize experimental time, we reduced the sweep-width and time-domain points while increasing the number of scans. Therefore, only 4 of 8 adenosine C2-H2 resonances were resolved (Supplementary Fig. S4). Nevertheless, $R_{1,C2\text{(uniform)}}$ was again observed to be significantly higher than $R_{1,C2\text{(selective)}}$ for all 4 resolved HBV $\varepsilon$ adenosine residues (Fig. 3a). Moreover, the average percent difference in measured $R_{1,C2}$ at 5 °C was significantly higher than those measured at 25 °C (Fig. 3b), in agreement with our simulations (Fig. 1b). Specifically, the average percent difference in measured $R_{1,C2}$ rates was 25.5% (Fig. 3b), compared to the simulated 15.6% (Fig. 1b) for an RNA with a $\tau_c$ of 21 ± 1 ns at 800 MHz (measured from $R_2/R_1$ (Fushman et al. 1994; Thakur et al. 2010)) (Supplementary Fig. S3).

Taken together, while relatively isolated, adenosine C2 experiences long-range $^{13}C\cdot^{13}C$ dipolar couplings that can neither be wholly ignored nor circumvented with selective pulses in [U-13C/15N]-ATP labeled samples. That is, these dipolar contributions must be explicitly taken into account.
Adenosine $C_2 R_{1p}$ relaxation and steady-state $^{13}C\{^{1}H\}$ hNOE measurements in uniformly and selectively labeled RNA

As previously described, $R_1$, $R_2$, and hNOE measurements are a prerequisite to a robust analysis of RNA ps-ns dynamics (Marušič et al. 2019; Palmer 2004; Wagner 1993; Lipari and Szabo 1982). We have already quantified the discrepancies that exist in adenosine $R_{1,C2}$ measurements derived from [$U-$13C/15N]-ATP labeling. While we did not observe such differences in the simulated adenosine $R_{2,C2}$ rates or steady-state $^{13}C\{^{1}H\}$ hNOE values (Supplementary Fig. S2), we sought to experimentally verify this for completeness. We therefore measured adenosine $R_{2,C2}$ rates and $^{13}C\{^{1}H\}$ hNOE values for [$U-$13C, 7-15N]-ATP labeled HBV ε (Fig. 2) at 800 MHz and 25 °C using TROSY-detected pulse sequences (Hansen and Al-Hashimi 2007; Lakomek et al. 2013; Akke and Palmer 1996; Peng et al. 1991; Korzhnev et al. 2002) to extract $R_2$ rates in HBV ε. In agreement with our simulations, adenosine $R_{2,C2}$ rates and steady-state $^{13}C\{^{1}H\}$ hNOE values did not differ significantly between uniformly or selectively labeled samples (Supplementary Fig. S5). For straightforward analysis, we will interpret dynamics data from our [2-13C, 7-15N]-ATP labeled sample. As such, adenosine $R_{1,C2}$ and $R_{2,C2}$ rates measured in helical regions of HBV ε were all close to the mean, except for residues A13 and A21 (Fig. 4). Specifically, residue A13 shows high $R_{1,C2}$ and low $R_{2,C2}$ rates suggestive of increased internal motions (Fig. 4). Residue A21, on the other hand, has a high $R_{2,C2}$ rate indicative of possible $R_{ex}$ contributions (Fig. 4). In addition to $R_1$ and $R_2$ rates, accurate measurements of steady-state $^{13}C\{^{1}H\}$ hNOE values can provide further information on RNA dynamics (Marušič et al. 2019; Palmer 2004; Wagner 1993; Lipari and Szabo 1982). Consistent with adenosine $R_{1,C2}$ and $R_{2,C2}$ rates, residue A13 shows the highest hNOE value suggestive of increased internal motions (Fig. 4). All other adenosine C2 nuclei have hNOE values close to the mean indicative of helical residues (Fig. 4). Taken together, our simulations and experimental measurements suggest that the discrepancy between $R_{1,C2}\{^{unif}\}$ and $R_{1,C2}\{^{select}\}$ increases with higher molecular weights.

$$\theta = \tan^{-1}\left(\frac{\omega_1}{\Omega}\right). \quad (8)$$

Here, $\omega_1$ is the strength of the spin-lock field and $\Omega$ is the offset from the spin-lock carrier frequency. We used an $R_{1p}$ experiment (Hansen and Al-Hashimi 2007; Lakomek et al. 2013; Akke and Palmer 1996; Peng et al. 1991; Korzhnev et al. 2002) to extract $R_2$ rates in HBV ε. In agreement with our simulations, adenosine $R_{2,C2}$ rates and steady-state $^{13}C\{^{1}H\}$ hNOE values did not differ significantly between uniformly or selectively labeled samples (Supplementary Fig. S5). For straightforward analysis, we will interpret dynamics data from our [2-13C, 7-15N]-ATP labeled sample.

The rate $R_{1p}$ is a function of $R_1$ and $R_2$ relaxation, which is accounted for according to the relations (Hansen and Al-Hashimi 2007; Lakomek et al. 2013; Akke and Palmer 1996; Davis et al. 1994)

$$R_{1p} = R_1(\cos^2\theta) + R_2(\sin^2\theta) \quad (7)$$

(Hansen and Al-Hashimi 2007) when interpreting adenosine $R_{1,C2}$ rates in terms of motional models for large RNAs.

![Fig. 3](image-url) Experimental adenosine $R_{1,C2}$ measurements in [$U-$13C/15N]-ATP or [2-13C, 7-15N]-ATP labeled HBV ε RNA. a. Adenosine $R_{1,C2}\{^{unif}\}$ and $R_{1,C2}\{^{select}\}$ rate measurements in HBV ε at 800 MHz and 5 or 25 °C. Mean rates are shown with dashed lines and error bars represent ± standard deviation (s.d.). Experimental $R_{1,C2}\{^{unif}\}$ rates at 25 °C were larger (outside experimental error) than $R_{1,C2}\{^{select}\}$ for all adenosine residues except A29 and A55 (designated no significance, n.s.). Experimental $R_{1,C2}\{^{unif}\}$ rates at 5 °C were larger than $R_{1,C2}\{^{select}\}$ for all 4 resolved adenosine residues. b. Average $R_{1,C2}$ Percent difference (diff.) [100*(R_{1,C2}\{^{unif}\} - R_{1,C2}\{^{select}\})/R_{1,C2}\{^{unif}\}] for the data at different temperatures (temp.) shown in a. The average percent difference in measured $R_{1,C2}$ rates at 25 °C was 4.7%, which agrees well with the simulated 5.4% difference for an RNA with a $\tau_C$ of 11 ± 1 ns [measured from $R_2/R_1$ ratio (Fushman et al. 1994; Thakur et al. 2010)]. The average percent difference in measured $R_{1,C2}$ rates at 5 °C was 25.5%, compared to the simulated 15.6% difference for an RNA with a $\tau_C$ of 21 ± 1 ns [measured from $R_2/R_1$ ratio (Fushman et al. 1994; Thakur et al. 2010)]. Taken together, our simulations and experimental measurements suggest that the discrepancy between $R_{1,C2}\{^{unif}\}$ and $R_{1,C2}\{^{select}\}$ increases with higher molecular weights.
relaxation measurements in HBV ε without the need for selective pulses (Emsley and Bodenhausen 1992; Kupče et al. 1995; Geen and Freeman 1991) or explicit spectral density modeling with assumed models of motion (Hansen and Al-Hashimi 2007). As an added benefit, 1H-13C TROSY spectra collected on selectively labeled HBV ε showed better signal-to-noise and narrower 1H linewidths compared to its [U-13C/15N]-ATP counterpart (Supplementary Fig. S6).

**Conclusion**

We investigated and quantified the effect of long-range 13C-13C dipolar couplings on adenosine C2 relaxation in [U-13C/15N]-ATP and [2-13C, 7-15N]-ATP labeled RNAs. Selective 13C-labeling of adenosine C2 removed unwanted dipolar interactions with C4, C5, and C6 found in [U-13C/15N]-ATP. Theoretical simulations and experimental measurements revealed non-negligible overestimates in adenosine R1,C2 rates derived from [U-13C/15N]-ATP labeled samples that increase with higher magnetic fields and molecular weights. The agreement between our experimental and simulated R1,C2 rates and discrepancies at 25 °C support the predictions from our simulations. Moreover, R1,C2 measurements at 5 °C (increased molecular weight) revealed exacerbated R2,C2 discrepancies, which further confirms our simulations and argues that selective 13C2 labeled probes simplify R1,C2 measurements in RNAs with a τC > 20 ns.

It is important to note that auto-relaxation due to the 13C-13C dipolar interaction does not lead to deviation from the expected monoexponential relaxation and can be explicitly taken into account by using the appropriate spectral density function (Hansen and Al-Hashimi 2007). Therefore, elimination of these unwanted 13C-13C dipolar contributions permits the use of simple spectral density modeling, offering advantages in data analysis. We also observed better signal-to-noise and narrower 1H linewidths in 1H-13C TROSY spectra collected on selectively labeled samples compared to its uniformly labeled counterpart. To take advantage of these benefits, our atom-selectively labeled [2-13C, 7-15N]-ATP was also used to measure 13C R1 relaxation rates and steady-state 13C{1H} hNOE values in HBV ε. These spin relaxation measurements provide a starting point to a robust understanding of HBV ε dynamics and suggest that residue A13 has increased flexibility whereas A21 may have R_ex contributions.

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**Data availability** All results generated in this study are included in this published article and its Supplementary Materials.

**Declarations**

**Conflict of interest** The authors declare no competing interests.

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![Fig. 4 Experimental adenosine C2 relaxation measurements for [2-13C, 7-15N]-ATP labeled HBV ε at 800 MHz and 25 °C. Adenosine R1,C2 and R2,C2 (calculated from R1ρ,C2 using Eqs. 6 and 7) rates and steady-state 13C{1H} hNOE measurements are shown. Error bars represent ± s.d. and the mean relaxation parameters are shown with dashed lines with a shaded box representing ± s.d. above and below the mean. Residue A13 shows high R1,C2 and hNOE suggestive of increased internal motions whereas A21 has a high R2,C2 rate indicative of possible R_ex contributions.](http://example.com)
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