Impact of Stokes Shift on the Performance of Near-Infrared Harvesting Transparent Luminescent Solar Concentrators

Chenchen Yang1, Jun Zhang2*, Wei-Tao Peng2, Wei Sheng2, Dianyi Liu1, Padmanaban S. Kuttipillai3, Margaret Young1, Matthew R. Donahue1, Benjamin G. Levine2*, Babak Borhan2 & Richard R. Lunt1,3

Visibly transparent luminescent solar concentrators (TLSC) have the potential to turn existing infrastructures into net-zero-energy buildings. However, the reabsorption loss currently limits the device performance and scalability. This loss is typically defined by the Stokes shift between the absorption and emission spectra of luminophores. In this work, the Stokes shifts (SS) of near-infrared selective-harvesting cyanines are altered by substitution of the central methine carbon with dialkylamines. We demonstrate varying SS with values over 80 nm and ideal infrared-visible absorption cutoffs. The corresponding TLSC with such modification shows a power conversion efficiency (PCE) of 0.4% for a >25 cm² device area with excellent visible transparency >80% and up to 0.6% PCE over smaller areas. However, experiments and simulations show that it is not the Stokes shift that is critical, but the total degree of overlap that depends on the shape of the absorption tails. We show with a series of SS-modulated cyanine dyes that the SS is not necessarily correlated to improvements in performance or scalability. Accordingly, we define a new parameter, the overlap integral, to sensitively correlate reabsorption losses in any LSC. In deriving this parameter, new approaches to improve the scalability and performance are discussed to fully optimize TLSC designs to enhance commercialization efforts.

Seamless installation of transparent luminescent solar concentrator systems onto the architectural envelope transforms passive surfaces into solar energy harvesting resources, dramatically improving energy utilization efficiency without compromising their current functionality and aesthetic quality underneath1-3. However, reabsorption of emitted photons combined with non-unity quantum yield (QY) of the luminophores act as the main loss mechanism that can dramatically limit the power conversion efficiency over larger areas (transparent, colored, or opaque). Reabsorption loss originates from the overlap between the absorption and emission spectra4,5. The Stokes shift (SS), defined as the wavelength difference between the absorption and emission peak maxima for the same transition, is frequently used to quantify and rationalize this loss in LSCs.

Recently, several approaches towards mitigating the reabsorption effect by increasing the Stokes shift with various species of luminophores have been reported for quantum dots1-7, rare-earth ions8-17, nanoclusters18-22, and organic molecules23-31. For example, inorganic semiconductor nanocrystals exhibit high photoluminescence efficiencies with absorption and emission spectra that are tunable by particle size and composition. Several strategies have been developed to increase the Stokes shift, including most notably the formation of core/shell “giant” quantum dots (QDs) as quasi-type I or type II hetero-structures for CdSe/CdS7,12, PbS/CdS14 or I-II-VI ternary CdSe/CdₓPb₁₋ₓS8, CuInS₂/CdS9, CuInS₂/ZnS QDs11. The nanocrystal shell typically has a larger energy bandgap, acting as a photon absorbing antenna and protective carrier barrier when energy is transferred to the lower bandgap core crystal photon emitter. The energy gap difference between the core and the shell crystals results in an increase in downshift up to 150–200 nm14. Doping quantum dots with transition metal ions is another approach to tackle the reabsorption problem, for example, utilizing Mn-doped ZnSe14, Cu-doped CdSe QDs or...
nanoplatelets. The doping impurity introduces new localized excited energy states (mid-gaps) within the original QD energy bandgap, which generates a downshifted radiative recombination with respect to the absorption.

However, a key limitation of these QDs is the continuous band-like absorption profiles that hinder selective absorption of invisible infrared photons without an accompanying absorption in the visible that reduce their transparency and aesthetic quality. In contrast, organic molecules are a class of luminophore candidates for LSC and TLSC applications that exhibit excitonic properties and separated molecular orbitals stemming from their \( \pi \)-conjugated molecular structure. While the Stokes shifts of traditional and commercially available organic dyes utilized in LSCs are generally small (<20–30 nm), recent efforts have looked to circumvent the reabsorption loss by using an excitation energy transfer (energy migration) strategy with multiple dyes via Förster resonance energy transfer (FRET). Such an approach separates the absorption of the donor from the emission of the acceptor so that the reabsorption in the LSCs is reduced but the close physical coupling of the dyes along with the need for multiple dyes with high quantum yields generates additional challenges. Another method has also been explored via resonance shifting in optical cavity designs for the waveguides, but it requires the utilization of neat thin-film layers of luminophores which are often less suitable for achieving the highest luminescent quantum yields.

For many TLSC applications, high aesthetic quality and transparency are the most critical metrics. Thus, harvesting the invisible portion of the solar spectrum (ultraviolet (UV) and near-infrared (NIR)) is most beneficial for such applications. TLSC with NIR selective harvesting cyanine dyes has been demonstrated in previous work but the Stokes shifts were all <30 nm, thus limiting the larger area optimization. In this work, we develop large Stokes shift TLSCs by modifying the central methine coordination of NIR selective cyanine dyes, resulting in Stokes shifts over 80 nm with simultaneously improved QY and maintaining selective NIR harvesting. These changes in SS are explained by ab initio calculations which show that the distortion about the central amino group in the excited states decreases the energy of the lowest unoccupied molecular orbitals (LUMO) energy. The corresponding TLSC devices exhibit a 30% PCE improvement for a 25.8 cm\(^2\) device that was found to stem, surprisingly, not from the changes in SS but from changes in the absorption width and improved quantum yield. These trends are quantitatively confirmed by distance dependence quantum efficiency measurements and optical modeling. Thus, we introduce a new parameter to replace the Stokes shift, the overlap integral, to more accurately correlate the true reabsorption loss, act as a fast screening parameter, and prevent misleading expectations in performance. In deriving this new parameter, approaches towards minimizing the loss to reabsorption are proposed as a roadmap for both LSC and TLSC designs to help realize their full potential.

We focus on two key parent cyanine salts that are derivatized to modify the Stokes shift: 2-((E)-2-((E)-2-chloro-3-(2-((E)-1,3,3-trimethylindolin-2-ylidine)ethylidene)cyclohex-1-en-1-yl)vinyl)-1,3,3-trimethyl-3H-indol-1-ium iodide and 2-((E)-2-((E)-2-chloro-3-(1,1,3-trimethyl-1,3-dihydro-2H-benz[e]indol-2-ylidine)ethylidene)cyclohex-1-en-1-yl)vinyl]-1,3,3-trimethyl-3H-indol-1-ium iodide. These parent compounds are converted via the addition/elimination reaction of the CI on the central methine backbone to 2-((E)-2-((E)-2-((E)-2-chloro-3-(2-((E)-1,3,3-trimethylindolin-2-ylidine)ethylidene)cyclohex-1-en-1-yl)vinyl)-1,3,3-trimethyl-3H-indol-1-ium iodide (Cy7-NEt\(_2\)-I) and 2-((E)-2-((E)-2-((E)-2-chloro-3-(3-ethyl-1,1-dimethyl-1,3-dihydro-2H-benz[e]indol-2-ylidine)ethylidene)cyclohex-1-en-1-yl)vinyl]-3-ethyl-1,1-dimethyl-1H-benz[e]indol-3-ium iodide (Cy7.5-NEt\(_2\)-I). In addition, 1-(5-carboxypentyl)-3,3-dimethyl-2-(((E)-2-((E)-3-(3-ethyl-1,1-dimethyl-1,3-dihydro-2H-benz[e]indol-2-ylidine)ethylidene)cyclohex-1-en-1-yl)vinyl)-3H-indolium chloride (Cy7-CA) introduced previously is also included for comparison. We have tested a large number of different substituents, substituted at C40 with SS ranging from <20 nm to >180 nm. The result of those studies is described in more detail elsewhere; in this work, we focus on these two particular derivaties for device integration as they provided the highest SS and QY with selective absorption in NIR range of the solar spectrum. The absorption and emission spectra in both dichloromethane (DCM) solution and in a polymer matrix of Cy7-CA, Cy7-NEt\(_2\)-I and Cy7.5-NEt\(_2\)-I are plotted in Fig. 1c–e. The truncated molecular structures of all three cyanine dyes are shown in Fig. 2. Cy7-CA acts as the control luminophore with a small Stok’s shift of 27 nm in DCM. The Stokes shift of the diethylamino substituted analog, Cy7-NEt\(_2\)-I is increased to 84 nm with a QY of 30 ± 2% and absorption peak of 700 nm in DCM. Similarly, the modified Cy7.5-NEt\(_2\)-I also shows an increased SS of 81 nm with red-shifted absorption peak of 738 nm compared to Cy7-NEt\(_2\)-I. The QYs of these three cyanine dyes are summarized in Table 1 where the QY of the three cyanine dyes in the polymer film are modestly reduced compared to that in DCM solution. Density functional theory based calculations shown in Fig. 2 are utilized to understand the mechanism of the Stokes shift variation. The NEt\(_2\) substitution leads to additional modestly reduced compared to that in DCM solution. Density functional theory based calculations shown in Fig. 2 are utilized to understand the mechanism of the Stokes shift variation. The NEt\(_2\) substitution leads to additional...
**Figure 3.** The measured short-circuit current density ($J_{SC}$) of the device with Cy7-NEt$_2$-I is 1.18 mA cm$^{-2}$, with an open-circuit voltage ($V_{OC}$) of 0.51 V and a fill factor ($FF\%$) of 60% leading to an efficiency of 0.36%. The $J$-$V$ characteristic of TLSC with Cy7-CA shows a $J_{SC}$ of 0.93 mA cm$^{-2}$, with a $V_{OC}$ of 0.49 V and $FF\%$ of 61%, resulting in a $PCE$ of 0.28%, which is lower than previously reported Cy7 devices due to the 6-times larger device area.

**Figure 1.** (a) Schematic showing a transparent luminescent solar concentrator (LSC) that selectively harvests near-infrared (NIR) light and emits deeper NIR while passing visible light. (b) Photographs of the TLSCs in front of the MSU Spartan helmet incorporating Cy7-CA, Cy7-NEt$_2$-I and Cy7.5-NEt$_2$-I luminophores (illuminated from behind the TLSC). Normalized absorption (blue) and emission spectra (red) of Cy7-CA (c) Cy7-NEt$_2$-I (d) and Cy7.5-NEt$_2$-I (e) in DCM solutions (solid lines) and polymer films (dashed lines). Permission to utilize the Spartan helmet logo is kindly provided by MSU.

**Figure 2.** Molecular structure, HOMO and LUMO electronic orbitals of Cy7-CA (a) Cy7-NEt$_2$-I (b) and Cy7.5-NEt$_2$-I (c).
While Cy7-NEt2-I with the highest absorption wavelength range of these three cyanine dyes yields an integrated EQE of the edge-mounted PV cell over the emission wavelength range of these three cyanine dyes, QY yields an integrated source to edge-mounted PV cell. Based on its wide absorption and high transmission (1−R(λ)), the Cy7.5-NEt2-I matches the absorption spectra in Fig. 1c,e and no direct excitation of the second cyanine luminophore derivative Cy7.5-NEt2-I has similar absorption (1.02 mA cm−2) and an overall efficiency of 0.28% which is similar to the Cy7-CA control TLSC device. Figure 3b shows the external quantum efficiency (EQE) spectra of the three cyanine luminophores (see Experimental Section for details of the measurements). In general, the absorption spectra of the luminophores determine where the EQE peaks will be. This can be calculated as:

$$\text{EQE}_{\text{LSC}}(\lambda) = \eta_{\text{eq}}(\lambda) \frac{\int \text{EQE}_{\text{PV}}(\lambda') \text{PL}(\lambda') d\lambda'}{\int \text{PL}(\lambda') d\lambda'}$$

(1)

where EQE_{LSC}(\lambda) is the EQE spectrum of the LSC system, which is the product of the LSC optical efficiency \(\eta_{\text{eq}}(\lambda)\) at the absorption wavelength of the luminophore and the EQE of the edge-mounted PV cell over the emission wavelengths of the luminophore. To avoid confusion, it should be noted that the integrals here are performed over the wavelength range of the PL of the emission (\(\lambda\)) not the wavelength of the incident light (\(\lambda\)). The peak positions of Cy7-CA, Cy7-NEt2-I and Cy7.5-NEt2-I match the absorption spectra in Fig. 1c−e and no direct excitation of the edge mounted solar cells is observed in the spectra. In the emission wavelength range of these three cyanine dyes (700 to 850 nm) the edge-mounted Si PV show a nearly constant EQE (~90%) so that Eq. 1 simplifies to

$$\text{EQE}_{\text{LSC}}(\lambda) = \eta_{\text{eq}}(\lambda) \cdot \text{EQE}_{\text{PV}}$$

where EQE_{PV}(\lambda) = \int \text{EQE}_{\text{PV}}(\lambda') \text{PL}(\lambda') d\lambda' / \int \text{PL}(\lambda') d\lambda'.

Table 1. Summary of the absorption \(\lambda_{\text{max}}\), emission \(\lambda_{\text{max}}\), Stokes shifts (SS) and quantum yields (QYs) of Cy7-CA, Cy7-NEt2-I and Cy7.5-NEt2-I in DCM and polymer films.

|       | Absorption \(\lambda_{\text{max}}\) (nm) | Emission \(\lambda_{\text{max}}\) (nm) | SS (nm) | QY (%) |
|-------|----------------------------------------|-------------------------------------|---------|--------|
| Cy7-CA | 760 (1.631 eV)                         | 787 (1.575 eV)                      | 27      | 24 ± 1 |
|       | 762 (1.627 eV)                         | 788 (1.573 eV)                      | 26      | 19 ± 1 |
| Cy7-NEt2-I | 780 (1.771 eV)                         | 784 (1.581 eV)                      | 84      | 30 ± 2 |
|       | 710 (1.746 eV)                         | 780 (1.590 eV)                      | 70      | 26 ± 1 |
| Cy7.5-NEt2-I | 738 (1.680 eV)                        | 819 (1.514 eV)                      | 81      | 23 ± 1 |
|       | 746 (1.662 eV)                         | 816 (1.519 eV)                      | 70      | 15 ± 1 |

Figure 3. Current density as a function of voltage (J−V curves) for the fully assembled TLSC systems with three of the cyanine dyes based on waveguide dimension of 5.08 cm × 5.08 cm. (b) Representative external quantum efficiency (EQE) of three cyanine dye TLSC systems as a function of wavelength (measured at distance \(d = 5 \text{ mm})\). (c) J−V curves for the fully assembled TLSC systems with three of the cyanine dyes based on waveguide dimension 2.54 cm × 2.54 cm.

Second cyanine luminophore derivative Cy7.5-NEt2-I has similar \%SC of 0.48 V and FF% of 57% with lower \(J_{\text{SC}}\) of 1.02 mA cm−2, and an overall efficiency of 0.28% which is similar to the Cy7-CA control TLSC device. Figure 3b shows the external quantum efficiency (EQE) spectra of the three cyanine luminophores. In general, the absorption spectra of the luminophores determine where the EQE peaks will be. This can be calculated as:

$$\text{EQE}_{\text{LSC}}(\lambda) = \eta_{\text{eq}}(\lambda) \frac{\int \text{EQE}_{\text{PV}}(\lambda') \text{PL}(\lambda') d\lambda'}{\int \text{PL}(\lambda') d\lambda'}$$

(1)

where EQE_{LSC}(\lambda) is the EQE spectrum of the LSC system, which is the product of the LSC optical efficiency \(\eta_{\text{eq}}(\lambda)\) at the absorption wavelength of the luminophore and the EQE of the edge-mounted PV cell over the emission wavelengths of the luminophore. To avoid confusion, it should be noted that the integrals here are performed over the wavelength range of the PL of the emission (\(\lambda\)) not the wavelength of the incident light (\(\lambda\)). The peak positions of Cy7-CA, Cy7-NEt2-I and Cy7.5-NEt2-I match the absorption spectra in Fig. 1c−e and no direct excitation of the edge mounted solar cells is observed in the spectra. In the emission wavelength range of these three cyanine dyes (700 to 850 nm) the edge-mounted Si PV show a nearly constant EQE (~90%) so that Eq. 1 simplifies to

$$\text{EQE}_{\text{LSC}}(\lambda) = \eta_{\text{eq}}(\lambda) \cdot \text{EQE}_{\text{PV}}$$

where EQE_{PV}(\lambda) = \int \text{EQE}_{\text{PV}}(\lambda') \text{PL}(\lambda') d\lambda' / \int \text{PL}(\lambda') d\lambda'.

The wider absorption peak of Cy7.5-NEt2-I compensates the slightly lower \(J_{\text{SC}}\) compared to Cy7-CA. All the integrated \(J_{\text{SC}}\) values are within error of the photocurrent densities from J−V measurement. To check the validity of photon balance from the EQE, transmission (\(T(\lambda)\)), and reflection (\(R(\lambda)\)) spectra measurements of these devices, we show that EQE(\lambda) + R(\lambda) + T(\lambda) ≤ 1 is satisfied at each wavelength39. This validity check is plotted in Fig. S3 for each device. It is also worth noting that the TLSC devices with these three cyanine dyes have been made with a smaller active area (6.45 cm2) similar to prior work utilizing 1-(6-(2,5-dioxopyrrolidin-1-ylloxy)-6-oxohexyl)-3,3-dimethyl-2-((E)-2-((E)-3-((E)-2-(1,3,3 trimethylindolin-2-ylidene)ethylidene)cyclohex-1-enyl)
vinyl)-3H-indolium chloride (Cy7-NHS) that had an active area of 4 cm² (Fig. 3 (c)). With similar device active area, the smaller TLSC with Cy7-NEt₂-I exhibit significantly improved PCE of 0.62% (2.21 mAcm⁻², 0.47 V of VOC and 60% of FF%) over previous work, while the TLSCs with the two other cyanine dyes, Cy7-CA and Cy7.5-NEt₂-I, have very similar photovoltaic performance (PCE ~0.4%) compared to previous work (Table 2).3

To explore the impact of Stokes shift on the scalability, TLSC systems were characterized by the external quantum efficiency as a function of position. Multiple EQE scans were taken for each TLSC system as d was increased from 15 mm to 95 mm (10 mm interval, and the same Si PV strip was used for all the EQE scans). The normalized EQE spectra of three cyanine dyes were plotted in Fig. 4a–c. The EQE peak values of each individual scan of the three cyanine dyes were extracted and plotted in Fig. 4d.

The overall power conversion efficiency of an LSC or TLSC system is the product of the component efficiencies:4

\[
\text{PCE} = \text{Area} \times \text{Jsc} \times \text{Int. Jsc} \times \text{Voc} \times \text{FF} \times \text{PCE} \times \text{AVT} \times \text{CRI} \times \text{S} \times \text{S'} \times \text{OI}
\]

### Table 2.

| Cyanine Luminophore | Area (cm²) | Jsc (mAcm⁻²) | Int. Jsc (mAcm⁻²) | Voc (V) | FF (%) | PCE (%) | AVT (%) | CRI | J(µm³M⁻¹) | S | S' | OI |
|---------------------|-----------|--------------|-------------------|---------|--------|---------|---------|-----|-----------|---|----|----|
| Cy7-NHS             | 4         | 1.2 ± 0.1    | 1.00              | 0.50 ± 0.01 | 66 ± 2 | 0.40 ± 0.03 | 87.7 | 91.0 | 1.49      | 4.07 | 1.84 | 27.9 |
| Cy7-CA              | 6.45      | 1.55 ± 0.05  | 0.96              | 0.47 ± 0.01 | 61 ± 1 | 0.44 ± 0.02 | 88.1 | 92.1 | 1.56      | 3.49 | 1.72 | 27.2 |
| Cy7-NEt₂-I          | 25.8      | 0.93 ± 0.02  | 0.49 ± 0.01       | 61 ± 1   | 0.28 ± 0.02 | 77.1 | 75.6 | 0.46      | 10.22 | 3.42 | 25.9 |
| Cy7.5-NEt₂-I        | 25.8      | 2.2 ± 0.2    | 1.22              | 0.47 ± 0.01 | 60 ± 1 | 0.62 ± 0.05 | 84.7 | 89.4 | 0.99      | 7.22  | 2.82  | 30.8 |

Figure 4. Position-dependent EQE of Cy7-CA (a), Cy7-NEt₂-I (b) and Cy7.5-NEt₂-I (c) as a function of wavelength measured from 15 mm to 95 mm, with 10 mm increments. (d) Calculated optical efficiencies (solid lines) as a function of distance d of three cyanine luminophore TLSC systems to fit the measured normalized EQE peak values (symbols).

To explore the impact of Stokes shift on the scalability, TLSC systems were characterized by the external quantum efficiency as a function of position. Multiple EQE scans were taken for each TLSC system as d was increased from 15 mm to 95 mm (10 mm interval, and the same Si PV strip was used for all the EQE scans). The normalized EQE spectra of three cyanine dyes were plotted in Fig. 4a–c. The EQE peak values of each individual scan of the three cyanine dyes were extracted and plotted in Fig. 4d.
where \( R_s \) is the front surface reflection, \( \eta_{abs} \) is the solar spectrum absorption efficiency of the luminophore, \( \eta_{PL} \) is the luminescence efficiency of the luminophore, \( \eta_{Trapp} \) is the photon trapping (or waveguiding) efficiency, \( \eta_{RA} \) is the efficiency of the edge-mounted PV cell normalized by its solar spectrum absorption efficiency and EQE at the luminophore wavelength to account for photon downshifting, and \( \eta_{Rf} \) is the efficiency of suppressing reabsorption.\(^{4,5,41}\) (see Supporting Information for details). We reemphasize that \( \eta_{opt}^{\lambda} = (1 - R_s) \cdot \eta_{abs} \cdot \eta_{PL} \cdot \eta_{Trapp} \cdot \eta_{RA} \cdot \eta_{Rf}^{\lambda} \) is the overall optical efficiency, which is defined as the ratio of number of photons reaching the waveguide front active surface across all incident wavelengths. In Eq. 1, \( \eta_{opt}^{\lambda} \) is the optical efficiency at a specific wavelength (\( \lambda \)) of the incident light utilized for quantum efficiency calculations so that \( \eta_{opt}^{\lambda} = (1 - R_s) \cdot \eta_{PL} \cdot \eta_{Trapp} \cdot \eta_{RA} \cdot \eta_{Rf}^{\lambda} \). Here, \( A(\lambda) \) is the normal incidence absolute absorption spectrum. It is assumed that all the other loss factors (\( \eta_{opt} \), \( \eta_{Trapp} \), and \( \eta_{RA} \)) are essentially independent of wavelength. Both optical efficiencies (\( \eta_{opt}^{\lambda} \) and \( \eta_{opt}^{\lambda} \)) have similar roll-off behavior as a function of distance (\( d \)), since both are predominantly limited by reabsorption loss.

The higher degree of conjugation with Cy7.5-NEt2-I results in a lower bandgap. Therefore, both the absorption and emission spectra of Cy7.5-NEt2-I are red-shifted compared to Cy7-NEt2-I, and the shape of both spectra remain nearly identical. That the absorption spectrum of Cy7-NEt2-I is blue-shifted relative to Cy7-CA can be understood via the Dewar-Knott color rule\(^{42–44}\). Addition of an electron donating species to the central position of the ethine chains of all three molecules relax similarly in the excited state, with individual bond lengths changing by up to 0.02 Å. Additional relaxation is observed in the central amino groups of Cy7-NEt2-I and Cy7.5-NEt2-I. The bond lengths between the central carbon of the polymethine chain and the amine nitrogen are lengthened by 0.02 Å, consistent with excitation into a LUMO that is antibonding with respect to the amine bond (Fig. 2). The amino group also twists relative to the polymethine chain upon excitation, with the torsion angles increasing from 44° to 55° in Cy7-NEt2-I and from 44° to 56° in Cy7.5-NEt2-I. This torsional motion reduces the conjugation of the lone pair on the nitrogen atom of the amino group to the \( \pi \) orbitals of the polymethine chain, thus decreasing the electron donating ability of the group. Together, these twisting and stretching motions destabilize the LUMO but leave the energy of the HOMO—which does not have density on the amine bond—relatively unaffected. These changes in orbital energy account for the enhanced Stokes shifts of Cy7-NEt2-I and Cy7.5-NEt2-I compared to Cy7-CA.

The nuclear relaxation responsible for the enhanced Stokes shift of Cy7-NEt2-I and Cy7.5-NEt2-I compared to Cy7-CA was investigated via linear response time-dependent density functional theory calculations. The computed Stokes shifts (0.07, 0.15, and 0.17 eV for truncated models of Cy7-CA, Cy7.5-NEt2-I, and Cy7.5-NEt2-I, respectively) are in good agreement with the experimental values (0.06, 0.19, and 0.17 eV in solution). The polymethine chains of all three molecules relax similarly in the excited state, with individual bond lengths changing by up to 0.02 Å. Additional relaxation is observed in the central amino groups of Cy7-NEt2-I and Cy7.5-NEt2-I. The bond lengths between the central carbon of the polymethine chain and the amine nitrogen are lengthened by 0.02 Å, consistent with excitation into a LUMO that is antibonding with respect to the amine bond (Fig. 2). The amino group also twists relative to the polymethine chain upon excitation, with the torsion angles increasing from 44° to 55° in Cy7-NEt2-I and from 44° to 56° in Cy7.5-NEt2-I. This torsional motion reduces the conjugation of the lone pair on the nitrogen atom of the amino group to the \( \pi \) orbitals of the polymethine chain, thus decreasing the electron donating ability of the group. Together, these twisting and stretching motions destabilize the LUMO but leave the energy of the HOMO—which does not have density on the amine bond—relatively unaffected. These changes in orbital energy account for the enhanced Stokes shifts of Cy7-NEt2-I and Cy7.5-NEt2-I compared to Cy7-CA.

The main factor that leads to enhanced performance for the TLSC with Cy7-NEt2-I is the increased \( J_{SC} \) (Table 2). Several key factors are responsible for these changes: changes in quantum yield, variations in total absorption (absorption width), and reductions in reabsorption loss. Surprisingly, the Cy7-NEt2-I with a large Stokes shift of 70 nm in the polymer film only shows slightly better reabsorption efficiency compared to Cy7-CA with a small Stokes shift of 26 nm, and Cy7.5-NEt2-I shows even more rapid EQE decay than the other two. To understand this surprising result, we remember that the EQE of TLSC consists of the optical efficiency, \( \eta_{opt} \) (the number of photons reaching the waveguide/number of photons incident on the waveguide active area) and the EQE of the PV at the emission wavelength. A numerical calculation of optical efficiency was performed by accounting for multiple reabsorption and emission events (see Supporting Information). Excellent agreement of the experimental EQE and the simulated optical efficiency suggests that reabsorption is indeed the main loss mechanism in all of these TLSC systems and that despite the large increase in the SS, the scalability is not significantly improved. Considering the other factors contributing to the photocurrent, it is primarily the increased absorption width and quantum yield that leads to the \( J_{SC} \) increase.

Both the experimental and modeling result suggests that Stokes shift is not ultimately a useful design parameter to identify how well a luminophore will perform in LSCs over large area. Here we define a new parameter, the overlap integral (OI) to quantify the reabsorption properties of a luminophore as:

\[
OI = \int_0^\infty A(\lambda) \cdot PL^*(\lambda) d\lambda
\]

where \( A(\lambda) \) is the absolute absorption spectrum (calculated by \( A(\lambda) = 1 - R(\lambda) - T(\lambda) \), \( R(\lambda) \) is the reflection spectrum, and \( T(\lambda) \) is the transmission spectrum) of a luminophore/host composite film, and \( PL^*(\lambda) \) is the normalized emission spectrum of the luminophore in the host material. The OI then depends on the thickness of the luminophore layer and the degree of overlap between the absorption and emission spectra in the host material (rather than in solution). The calculated OI for the investigated luminophores is summarized in Table 2. Despite the large SS between Cy7-CA and Cy7-NEt2-I and between Cy7-CA and Cy7.5-NEt2-I, there is only a small difference in the OI. This is because the absorption tail is broadened with the increase in the SS. Peak broadening is often observed with red-shifted chromophores, resulting from increased vibrational states and/or larger conformational flexibility and more potential isomeric states. Furthermore, a potential charge transfer process can also lead to spectral broadening, if a strong dipole is induced upon excitation. The similarity of the OI elucidates the...
similar optical efficiency (or EQE decay curves) in Fig. 4d and show the correct correlation: decreasing the OI leads to improved scalability in the EQE while the measured SS shows an incorrect trend. Thus, the OI more sensitively captures and reflects the distance dependence of luminophores with differing Stokes shifts. The way the OI is defined in Eq. 3 it is useful not only for organic dyes but all luminophores (including inorganic quantum dots) and all luminophore optical densities. For screening purposes the OI can be evaluated for fixed absolute peak (or specified wavelength) absorption values (e.g. $A = 80\%$). It is thus a useful design parameter for quickly tracking, predicting, and understanding relative performance changes in a range of LSC systems.

It is natural to consider the FRET overlap integral ($J$) as a parameter to correlate the EQE scalability as it is material specific. The well-known expression for $J$ is:

$$J = \frac{\int PL_d(\lambda)\epsilon_d(\lambda)\lambda^4 d\lambda}{\int PL_d(\lambda) d\lambda},$$

(4)

where $PL_d(\lambda)$ is the emission spectrum of the donor dye, and $\epsilon_d(\lambda)$ is the molar absorptivity coefficient of the acceptor dye. Conceptually, however, $J$ depends on both the shape and the magnitude of molar absorptivity coefficient ($\epsilon_d$) and therefore can predict the wrong scaling. For example, if the magnitude of $\epsilon_d$ is lower for the same spectral shape, one would simply load more luminophore to maintain the same optical density (absolute absorption) leading to the same OI but lower $J$. Indeed, we find that $J$ does not correlate with the scaling of the EQE with plate length. The measured trends, from lowest to highest scaling are: Cy7.5-NEt$_2$-I, Cy7-CA, Cy7-NEt$_2$-I; $J$ predicts Cy7-CA, Cy7.5-NEt$_2$-I, Cy7-NEt$_2$-I while the OI correctly captures the trend Cy7.5-NEt$_2$-I, Cy7-CA, Cy7-NEt$_2$-I. In addition to $J$, the parameter, $S$, has been defined previously to try to quantify the reabsorption loss behavior$^{35}$. This parameter was defined as the ratio of the absorption coefficients at the absorption and emission maxima in solution. We also defined a variation of the self-absorption ratio $S'$, defined as the ratio of the absolute absorption values at the absorption and emission maxima that can be used for solid films where there are subtle but important shifts in spectra. We calculate both $S$ and $S'$ for each luminophore (Table 2) and find not only do these parameters give opposing trends, neither accurately captures the observed scaling trend.

Given that the absorption coefficient in the NIR range for the host polymer material and targeted glass is in the range from $10^{-3}$ to $10^{-4}$ cm$^{-1}$ (e.g. poly(methyl methacrylate) and certain glasses) most reabsorption losses stems from the luminophore. To qualitatively connect the trends in the OI with the quantum efficiency roll-off behavior, we performed an additional simulation where the absolute absorption spectrum of a sample LSC was kept fixed and the normalized emission was manually shifted to create different overlap in the modeling as shown in Fig. 5a. We emphasize that while such a manual shifting of the emission corresponds to increases in the Stokes shift and creates different OI values, such an increase in the Stokes shift in practice does not necessarily lead to changes in the OI due to variations in the peak bandwidth. The calculated optical efficiency in Fig. 5b shows the impact of overlap integral on the TLSC scalability: if the OI can be decreased from 30 to 3 (i.e. an order of magnitude), the critical TLSC plate length ($L$) defined as the distance at which the optical efficiency decays to half of its original value can be increased from 2 cm to >1 m, which would be sufficient for many large-scale and window-based applications. We also note that there is a tradeoff between absorption efficiency and the OI on the total power conversion efficiency that also depends on the thickness (which dictates the optical density of the luminophore). In the case of the TLSCs, the impact on the average visible transparency (AVT) and color rendering index (CRI) should also be considered$^{39}$, emphasizing that broad absorption in the invisible solar spectrum with sharp absorption cutoffs around the visible and near the bandgap are also key. Thus, strategies for sharpening the densities of states around the bandgap should be explored moving forward. The most feasible approach to minimize OI is to modify the NIR selective harvesting luminophore so that both the absorption edges have sharp cutoffs, keeping the emission narrow as well. Adding more fused rings to lock the geometry of the cyanine dyes could potentially restrict the distribution of conformers at the ground state, and thus achieve sharper transition bandwidths. Furthermore, the restricted geometry (molecular rigidity) could lead to increased quantum efficiency and luminophore lifetime by reducing non-radiative decay pathways. The lifetime of cyanine dyes is another interesting and key area. The fabricated TLSC devices show no degradation during >2 hours in exposure to air. Interestingly, we have shown that the stability of such compounds integrated as active layers in photovoltaic devices (a more demanding application than LSCs) are more a function of the coordinating counterion than the photoactive counterion itself. We have shown that such anion modifications can lead to photovoltaic lifetime anywhere as short as few days to >7 years for the same photoactive cation$^{45}$. Thus, future efforts in characterizing the lifetime of these compounds in TLSC application will need to focus on both chemical modifications as well as ion pairing.

It is also important to consider the impact of increasing the OI by simply increasing the Stokes shift. The ideal Stokes shift should not only be engineered to minimize the OI but also carefully adjusted to allow all the emission of the luminophores to coincide with the high EQE wavelength range of the edge-mounted PV cells. If the SS is too large, a portion of the emission will have a wavelength longer than the absorption cut-off of the edge-mounted PVs and thus cannot be harvested. For example, with edge mounted Si PVs the maximum Stokes shift should be limited to <200 nm with the selective harvesting of a 200–300 nm slice of the NIR spectrum for optimal performance. For GaAs PVs with wider band gap the maximum Stokes shift is even more restricted.

In conclusion, we have synthesized novel NIR selective harvesting cyanine dyes with selective NIR harvesting, large Stokes shift >80 nm, and improved quantum yield of >30%. Luminescent solar concentrators based on these cyanine dyes exhibit power conversion efficiency of up to 0.6% combined with high visible transparency >80%. Based on the analysis of both experiment and simulation results, we show that the Stokes shift is not a suitable design parameter to quantify the reabsorption loss moving forward. Instead, we define a new parameter, the spectral “overlap integral”, derived in way to accurately capture the properties of the overlap between
absorption and emission of a luminophore in future LSC design and optimization. Simulations also indicates that with one order of magnitude decrease of the overlap integral the LSC plate size can be increased to ~1 m, which is sufficient for most structural glazing systems. Thus, this work provides a guide to improve the efficiency and scalability of NIR-selective harvesting TLSC systems (and all LSCs) that can help fulfill the promise of low cost transparent solar cells.

**Experimental Section**

**Module Fabrication.** 100 mgL⁻¹ Cy7-CA (150 mgL⁻¹ Cy7-NEt2-I or 150 mgL⁻¹ Cy7.5-NEt2-I) ethanol solution was mixed with mounting medium (Fluoroshield F6182, Sigma-Aldrich) at a volume ratio of 1:2. This mixture was drop-cast on 5.08 cm × 5.08 cm × 0.635 cm glass sheets (for photovoltaic characterization) twice and allowed to dry for 6h for each layer in a glove-box filled with nitrogen gas (O₂, H₂O < 1 ppm), resulting in a layer thickness of approximately 0.5 mm. Dichloromethane was mixed with (poly)-butyl methacrylate-co-methyl methacrylate (PBMMA) (Sigma-Aldrich) at a volume ratio of 1:1. This mixture was then drop cast onto the dye/Fluoroshield composite film to make a smooth and flat surface to avoid light scattering in the waveguide and act as a protection layer. The same layer structure was applied for 2.54 cm × 0.635 cm strips for photovoltaic characterization and 1.27 cm × 1.27 cm × 0.07 cm for QY measurements. For photovoltaic measurements, single-crystalline solar cells (Vikocell) were laser cut into 2.54 cm × 0.635 cm and 5.08 cm × 0.635 cm strips for PCE and EQE measurements and 10.16 cm × 0.635 cm strips for EQE versus SS measurements. For PCE measurements, two PV strips were mounted on orthogonal edges using index matching gel (Thorlabs) to attach the PV strips on glass edges seamlessly and were connected in parallel. The remaining two edges were covered with specular film reflector (DF2000MA series, 3 M). For EQE measurements, one PV strip was attached to one edge of the waveguide with the other three edges painted black.

**Optical Characterization.** Specular transmittance of both solutions and films were measured using a dual-beam Lambda 800 UV/VIS spectrometer in the transmission mode. The PL for the three cyanine dyes in both solutions and polymer films were measured using a PTI QuantaMaster 40 spectrofluorometer with excitation at 675 nm for Cy7-CA, 650 nm for Cy7-NEt2-I and Cy7.5-NEt2-I. Quantum yield measurements were tested by using Hamamatsu QuantaTaurus fluorometer, excitation ranges in scan mode (10 nm per scan step) were adjusted to 700–750 nm for Cy7-CA, 650–700 nm for Cy7-NEt2-I and 680–730 nm for Cy7.5-NEt2-I. Six QY values were collected for each individual cyanine dye, and the reported QY for each cyanine dye in Table 1 was averaged from these six QY values with corresponding excitation wavelengths.

**Module Photovoltaic Characterization.** J-V measurements were obtained using a Keithley 2420 source measurement under simulated AM1.5G solar illumination (xenon arc lamp with the spectral-mismatch factor of 0.97 ± 0.03 for all the devices tested). The light intensity was calibrated with an NREL-calibrated Si reference cell with KG5 filter. For position-dependent EQE measurements, the excitation beam was obtained by directing chopped incident light from a quartz tungsten halogen lamp through a monochromator. EQE scans were performed by positioning the monochromatic excitation beam from a fiber perpendicular to the LSC waveguide front surface at various distances from a single edge-mounted Si PV cell. The measured EQE was corrected by the geometric factor, \( g = \frac{\pi \tan^{-1}(L/2d)}{d} \), which accounts for the different angle subtended by the solar cell at various distance \( d \), where \( L \) is the LSC plate length. Note both PCE and EQE measurements for each cyanine dye were tested by using the same TLSC to match the \( J_{SC} \) with the integrated \( J_{SC} \), and a matte black background was placed

---

**Figure 5.** (a) Different overlap integral (OI) values obtained by keeping the absolute absorption fixed and shifting the normalized emission spectrum of a luminophore (Cy7-CA). We note that the OI and SS are not typically equivalent because chemical changes that lead to changes in the SS also lead to spectral changes in the tail absorption. The SS values for the simulation are provided to emphasize the reason that this parameter has been misleadingly considered as a design parameter. (b) Optical efficiencies as a function of plate length \( L \) for different OI values.
on the back of the tested TLSC to eliminate the illumination from the environment or reflection (double pass) for both PCE and EQE measurements. We also utilize the same PV cells mounted around the edge to eliminate any PV-to-PV variations in performance.

**Optical Modeling.** The reabsorption and forward emission losses were estimated with luminophore (Cy7-CA) absorption, emission spectra, distance \(d\) and TLSC plate length \(L\). The TLSC system optical efficiencies, in considering reabsorption losses from the overlap in the absolute absorption and normalized emission spectra were numerically evaluated in Matlab as a function of distance \(d\), plate length \(L\), plate thickness \(t\), and dye/polymer film thickness \(t\). The complete equations used in the simulations are provided in the Supplemental Information.

**Electronic Structure Calculations.** The geometries of Cy7-CA, Cy7-NEt2-I, and Cy7.5-NEt2-I were optimized in their ground and first excited electronic states to elucidate the relaxation motions responsible for the enhanced Stokes shifts of Cy7-NEt2-I and Cy7.5-NEt2-I. The charged side chain on the Cy7-CA and two ethyl groups on the two nitrogen atoms terminating the polymethine backbone of Cy7.5-NEt2-I were replaced by methyl groups to reduce the cost of calculations. This is expected to have little effect on the Stokes shifts because the HOMO and LUMO do not extend to these side chains (as shown in Fig. 2). Calculations were performed at the linear response time-dependent density functional level of theory using the TeraChem software package.51–53. The CAM-B3LYP functional54 and 6–31 G* basis was used, and all calculations were performed in the gas phase. Though sometimes predicting inaccurate vertical excitation energies, TDDFT is known to give an accurate description of the shape of the excited state potential energy surface (e.g. SS)53. These calculations were enabled by the Extreme Science and Engineering Discovery Environment (XSEDE)52. Torsion angles are defined as the mean of the two C1-C2-N-C3 dihedral angles where C2 is the central carbon atom of the polymethine chain and N is the nitrogen of the amino group.

**References**

1. Debije, M. G. & Verbunt, P. P. C. Thirty Years of Luminescent Solar Concentrator Research: Solar Energy for the Built Environment. *Adv. Energy Mater.* 2, 12–35 (2012).
2. Zhao, Y. & Lunt, R. R. Transparent luminous solar concentrators for large-area solar windows enabled by massive stoke-shift nanocluster phosphors. *Adv. Energy Mater.* 3, 1143–1148 (2013).
3. Zhao, Y., Meek, G. A., Levine, R. G. & Lunt, R. R. Near-Infrared Harvesting Transparent Luminescent Solar Concentrators. *Adv. Opt. Mater.* 2, 606–611 (2014).
4. Yang, C. & Lunt, R. R. Limits of Visibly Transparent Luminescent Solar Concentrators. *Adv. Opt. Mater.* 5, 1600851 (2017).
5. Goetzberger, A. & Greube, W. Solar energy conversion with fluorescent collectors. *Appl. Phys.* 14, 123–139 (1977).
6. Erickson, C. S. et al. Zero-Reabsorption Doped-Nanocrystal Luminous Solar Concentrators. *ACS Nano* 8, 3461–3467 (2014).
7. Coropceanu, I. & Baswendi, M. Core/Shell Quantum Dot Based Luminous Solar Concentrators with Reduced Reabsorption and Enhanced Efficiency. *Nano Lett.* (2014).
8. Zhao, H. et al. Absorption Enhancement in “Giant” Core/Alloyed-Shell Quantum Dots for Luminous Solar Concentrator. *Small* n/a-n/a (2016).
9. Knowles, K. E., Kilburn, T. R., Alnate, D. G., McDowall, S. & Gamelin, D. R. Bright CuInS2/CdS nanocrystal phosphors for high-gain full-spectrum luminous solar concentrators. *Chem. Commun.* 51, 9129–9132 (2015).
10. Bergren, M. R. et al. High-Performance CuInS2 Quantum Dot Laminated Glass Luminous Solar Concentrators for Windows. *ACS Energy Lett.* 520–525 (2018).
11. Li, C. et al. Large Stokes Shift and High Efficiency Luminous Solar Concentrator Incorporated with CuInS2/ZnS Quantum Dots. *Sci. Rep.* 5, 17777 (2015).
12. Bradshaw, L. R., Knowles, K. E., McDowall, S. & Gamelin, D. R. Nanocrystals for Luminous Solar Concentrators. *Nano Lett.* 15, 1315–1323 (2015).
13. Li, Y., Miao, P., Zhou, W., Gong, X. & Zhao, X. N-doped carbon-dots for luminous solar concentrators. *J. Mater. Chem. A* 5, 21452–21459 (2017).
14. Zhou, Y. et al. Near-Infrared, Highly Efficient Luminous Solar Concentrators. *Adv. Energy Mater.* 6, 1501913 (2016).
15. Sharma, M. et al. Near-Unity Emitting Copper-Doped Colloidal Semiconductor Quantum Wells for Luminous Solar Concentrators. *Adv. Mater.* 29, 1700821 (2017).
16. Saengkerdsub, S., Im, H.-J., Willis, C. & Dai, S. Pechini-type in-situ polymerizable complex (IPC) method applied to the synthesis of Y2O3:Ln (Ln = Ce or Eu) nanocrystals. *J. Mater. Chem.* 14, 1207–1211 (2004).
17. Wang, T. et al. Luminous solar concentrator employing rare earth complex with zero self-absorption loss. *Sol. Energy* 85, 2571–2579 (2011).
18. Sheng, X. et al. Silicon-Based Visible-Blind Ultraviolet Detection and Imaging Using Down-Shifting Luminophores. *Adv. Opt. Mater.* 2, 314–319 (2014).
19. Ronda, C. R., Justel, T. & Nikol, H. Rare earth phosphors: fundamentals and applications. *J. Alloys Compd.* 275–277, 669–676 (1998).
20. Chengelis, D. A., Yingling, A. M., Badger, P. D., Shade, C. M. & Petoud, S. Incorporating Lanthanide Cations with Cadmium Selenide Nanocrystals: A Strategy to Sensitize and Protect Tb(III). *J. Am. Chem. Soc.* 127, 16752–16753 (2005).
21. Reisfeld, R. & Kalisky, Y. Nd3+ and Yb3+ germanate and tellurite glasses for fluorescent solar energy collectors. *Chem. Phys. Lett.* 80, 178–183 (1981).
22. Sun, L.-N. et al. Near-infrared luminescent mesoporous materials covalently bonded with ternary lanthanide [Er(III), Nd(III), Yb(III), Sm(III), Pr(III)] complexes. *Microporous Mesoporous Mater.* 98, 156–165 (2007).
23. Zhang, J., Badger, P. D., Geib, S. J. & Petoud, S. Sensitization of Near-Infrared-Emitting Lanthanide Cations in Solution by Troponoligand Ligands. *Angew. Chemie Int. Ed.* 44, 2508–2512 (2005).
24. Kuttipillai, P. S. et al. Phosphorescent Nanocluster Light-Emitting Diodes. *Adv. Mater.* 28, 320–326 (2016).
25. Sokolov, M. N. et al. Highly luminescent complexes with poly(St-Co-MMA) as fluorescent solar collectors and their field performance. *Polymer.* 24, 519–525 (2003).
Acknowledgements
C.Y., J.Z., B.B., and R.R.L. gratefully acknowledge support from the National Science Foundation under grant CBET-1702591. WT, F. and B. G. L gratefully acknowledge support for the computational work from the National Science Foundation under grant CHE-1565634. This work used the Extreme Science and Engineering Discovery Environment (XSEDE), which is supported by National Science Foundation grant number ACI-1548562 (allocation TG-CHE140101). This work is dedicated to the memory of Seth Olsen.

Author Contributions
C.Y., B.G.L., B.B. and R.R.L. designed the project. C.Y. conducted the device experiments and acquired the data. J.Z. and W.S. synthesized the organic cyanine dyes. W.P. and B.G.L. performed the density functional theory calculations. D.L., P.S.K. and M.Y. assisted with photovoltaic measurements and analysis. M.R.D. assisted with the photoluminescence and quantum yield measurements. All authors contributed to the writing of the manuscript.

Additional Information
Supplementary information accompanies this paper at https://doi.org/10.1038/s41598-018-34442-3.

Competing Interests: C.Y., J.Z., W.S., B.G.L. and B.R.L. have filed a provisional patent based on the work in this manuscript. R.R.L is a co-founder, advisor, and a minority owner of Ubiquitous Energy, Inc., a company working to commercialize transparent photovoltaic technologies. All other authors declare no competing financial interest.

Publisher’s note: Springer Nature remains neutral with regard to jurisdictional claims in published maps and institutional affiliations.

Open Access This article is licensed under a Creative Commons Attribution 4.0 International License, which permits use, sharing, adaptation, distribution and reproduction in any medium or format, as long as you give appropriate credit to the original author(s) and the source, provide a link to the Creative Commons license, and indicate if changes were made. The images or other third party material in this article are included in the article’s Creative Commons license, unless indicated otherwise in a credit line to the material. If material is not included in the article’s Creative Commons license and your intended use is not permitted by statutory regulation or exceeds the permitted use, you will need to obtain permission directly from the copyright holder. To view a copy of this license, visit http://creativecommons.org/licenses/by/4.0/.

© The Author(s) 2018