Efficiency of Indian banks with non-performing assets: evidence from two-stage network DEA

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Abstract
This paper addresses the concerns regarding the sustainability of the banking sector in India prompted by the recent unintended high level of non-performing assets (NPAs). It uncovers the linkage between NPAs and banking efficiency by integrating NPAs into the measurement of bank efficiency to provide a holistic efficiency profile of the Indian banking sector. We apply the general two-stage data envelopment analysis of Kao [16] by incorporating NPAs as an exogenous output from the first stage, and the empirical results identify an efficiency gap of 16.2% due to NPAs in the Indian banking sector for the year 2016. Further, it also documents that the efficiency gap/loss is increasing over the years and differs according to the shareholding pattern of the banks.

Keywords: General two-stage network DEA, Bank efficiency, India, Non-performing assets

JEL Classification: G21, P42, C14, C44

Introduction
In emerging economies, banks play a more prominent role in financial intermediation, along with carrying additional responsibility for attaining the government’s social objectives as well. This inevitable relationship between banking and economic development, the growth of the overall economy, is naturally related to the health of the banking sector. The recent global financial crisis highlighted the importance of a healthy banking system. It emphasized the focus on proper monitoring and performance evaluations of banks, as this can impact their overall efficiency, productivity, performance, and profit.

World over, non-performing asset (NPA) in the banking sector is growing, and higher NPA influences the price of loans and interest rates, which in return affects the confidence of investors, lenders, and depositors equally. While higher interest rates will directly impact the investors in need of loans for the creation of infrastructural and industrial projects, it also causes poor recovery of funds, which will affect the credit creation and revenue stream of the banks. The non-recovery of loans affects credit creation and further affects the financial soundness of an economy. So managing the NPAs and maintaining them within the tolerance level will decide the success of a bank. Proper monitoring of NPAs and performance evaluations are very important for banking, as this reflects the overall efficiency of banking. Therefore, it is necessary to investigate the role of NPAs in determining the efficiency and profitability of the banking system.

The financial system in India, similar to other emerging countries, is bank dependent, and banks hold a significant share of total financial assets in the system. It is also having a reasonably large share of public sector banking and a higher level of NPAs compared to the other emerging countries. Recently, the Indian banking system is witnessing a sharp increase in the gross NPA level, and the government-owned public sector banks are mostly responsible for the NPA problem. The Reserve Bank of India (RBI) Financial Stability Report of 2017 states that the public sector banks have 14.6% gross NPA to total...
management can concentrate on that particular process to improve the efficiency. The paper is structured as follows: “Literature” section provides a brief literature review on the efficiency measurement of banks. “Methodology” section discusses the methodological approach adopted for the analysis and explains the general two-stage network DEA model along with the data used. “Result and discussions” section discusses the empirical results and policy suggestions, while the final section derives conclusions and managerial implications.

**Literature**

In the literature, understanding market efficiency and its effects on financial stability constitutes the macropoint of view [9, 20, 23], while understanding the efficiency of individual business units is the core at the micro-level. The focus of this study is at the micro-level to measure the efficiency of Indian commercial banks by incorporating NPAs to assess its impact on the profits of banks.

Several studies analyzing the efficiency of the Indian banking system, with most of the studies adopting the data envelopment analysis (DEA) methodology. All these studies examined the efficiency levels, and no study has attempted to quantify the level of efficiency loss arising out of undesirable outcomes like the non-performing assets of the bank. Bhatthacharya et al. [5] analyzed the performance of Indian banks during the initial stages of the liberalization period. They found that the public sector banks were more efficient compared to private banks. Similarly, Das and Shanmugam [8] measured the efficiency of Indian banks during the reform period based on the panel stochastic frontier analysis. They demonstrated an improved efficiency of the public sector banks. Ray and Das [22] examined the cost and profit efficiency of Indian banks in the post-reform period. They found that the public sector banks perform better than the private sector banks in terms of efficiency. They also reveal that small banks operated below the efficiency frontier, thus implying that the ownership pattern of the banks influenced the efficiency level of banks.

In recent years, the efficiency levels of the public sector banks and the private banks are seen to be reversing, with private banks becoming more efficient compared to other public sector banks like the State Bank of India (SBI, including its associate banks). Tzeremes [26], while examining the efficiency of the Indian banking industry from 2004 to 2012 using the directional distance function, found that the financial crisis had hardly affected the efficiency of Indian banks. However, private banks performed better than the public and foreign banks.

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1 Government of India holds a major share in these banks.
Sandeepa and Gupta [24], in their analysis of the banking efficiency in the post-crisis period from 2009 to 2013, demonstrated that SBI and its associate banks obtained the highest efficiency scores compared to other banks. The Indian banking system, dominated by public sector banks, has undergone a substantial change in terms of restructuring, mergers, and recapitalization due to the persistent growth of non-performing assets (NPA). It often mentioned as being the harbinger of an impending crisis within the Indian financial system. Jayaraman and Srinivasan [15] provided a holistic analysis of the Indian banking efficiency using the Nerlovian methodology and concluded that the profit inefficiency of Indian banks is mainly because of allocative inefficiency. Further, the study stated that the role of profit inefficiency was more compared to the technical inefficiency.

The major drawback of all these studies is the fact that they have considered the efficiency measurement as a “black box” [19] is ignoring the internal structure of the banking process and its efficiency. All these studies considered the total loan outlay as an output in the efficiency measurement of banks without considering that the loans generated consist of both good and bad loans. Färe et al. [10] argued that it is better to treat desirable and undesirable outputs asymmetrically in the efficiency measurement—where firms with bad outputs are penalized, and firms with desirable outputs are credited.

Chang [6] analyzed the efficiencies of major financial intermediaries in rural Taiwan. Incorporating risk such as non-performing loans (NPL), allowance for loan losses, and risky assets as an undesirable output demonstrated that an undesirable output has a significant impact on the efficiency ranking. Akhter et al. [1] evaluated the performance of the commercial banks in Bangladesh using the two-stage network DEA production process. Their findings suggest that non-performing loans (NPL) created in the previous period correspond with a reduction in the subsequent period’s production possibilities, as NPLs require the banks to either increase equity capital or contract deposit generation. Fukuyama and Weber [12] analyzed the inefficiency level of the Japanese banks by keeping NPLs as an undesirable output while using dynamic network DEA methodology. Their study established that there is higher inefficiency, which is mainly attributed to NPLs. Partovia and Matousek [21] studied the efficiency of Turkish banks from 2002 to 2017, applying a modified data envelopment analysis (DEA) method that used a directional distance function model to estimate the efficiency, where they considered NPLs as an undesirable output. The study indicates that the NPLs are severely affecting the efficiency of banks.

In recent years, there have been a few studies that analyzed the efficiency in the intermediation and operating stages using a two-stage network DEA framework. Fujii et al. [11] evaluated the technical efficiency and productivity growth in the Indian banks using a weighted Russell directional distance model by modifying and extending the methodological approaches of Chen et al. [7] and Barros et al. [2]. Their analysis observed that NPAs are the main reason for bank inefficiency.

Further, Gulati and Kumar [13] used the two-stage network DEA and suggested that the Indian banks have to improve both resource utilization and income-generating abilities to experience an overall improvement in efficiency. However, this study differs from the earlier ones by quantifying the efficiency gain/loss by incorporating NPAs in the analysis. It helps us to understand the banks that are weighed down by these NPAs on the efficiency front and identify some important factors that can move the banking sector forward and away from the clutches of NPAs.

**Methodology**

In the empirical literature, the technical efficiency of the banks is measured using either the production or the intermediation approaches. The production approach considers banks as a producer of services like deposits and loans with labor and capital as primary inputs. Intermediation approach considers banks as an agent to convert the deposits and other funds into loans and other assets. The debate on the “deposit dilemma” in the literature acknowledges whether the deposits (or raised funds) should be considered as an input or an output in measuring the banking efficiency. However, many studies adopting the conventional DEA method used deposits as an input as well as an output without discussing the issue of “deposit dilemma.” Some studies using two-stage network model have used the deposits as output in the first stage of the production and as an input in the second stage of the production. This study applies the intermediation approach of Berger and Mester [4].

First, we use a standard two-stage network DEA of Kao and Hwang [17] to derive the system and divisional efficiency scores for the actual data considering all the outputs in stages 1 and 2 as desirable outputs. Subsequently, the undesirable exogenous output from stage 1 is introduced in the general two-stage network DEA framework explained below to derive the system and its divisional efficiency scores. We define the efficiency gap (gain/loss) of that undesirable output as the difference between the system efficiency scores of the standard and the general models.
Two-stage DEA

For $N$ number DMUs (decision making units) DMU$_j$, $j = 1 \ldots N$, is based on the CRS (constant returns-to-scale) production process with $i$th input and $r$th output $X_{ri} = 1 \ldots m$ and $Y_{rj} = 1 \ldots s$, Kao and Hwang [17] proposed a two-stage network DEA model derived as the following linear program:

$$
E_k = \max \left( \sum_{r=1}^{s} u_r Y_{rk} \right) \quad \text{s.t.} \quad \sum_{i=1}^{m} v_i X_{ik} = 1,
$$

$$
\sum_{r=1}^{s} u_r Y_{rj} - \sum_{i=1}^{m} v_i X_{ij} \leq 0, \quad \sum_{p=1}^{q} w_p Z_{pj} - \sum_{i=1}^{m} v_i X_{ij} \leq 0,
$$

$$
\sum_{r=1}^{s} u_r Y_{rj} - \sum_{p=1}^{q} w_p Z_{pj} \leq 0, \quad \text{for } j = 1 \ldots n;
$$

$$
u_r, v_i, w_p \geq s, \quad r = 1 \ldots s, \quad i = 1 \ldots m, \quad p = 1 \ldots q.
$$

After the optimal multipliers $u^*_r, v^*_i$ and $w^*_p$ are solved, the system and divisional efficiencies are calculated as

$$
E_k = \sum_{r=1}^{s} u_r Y_{rk}, \quad E^1_k = \sum_{p=1}^{q} w_p Z_{pk}/\sum_{i=1}^{m} v_i X_{ik}
$$

and

$$
E^2_k = \sum_{r=1}^{s} u_r Y_{rj}/\sum_{p=1}^{q} w_p Z_{pj};
$$

this implies $E_k = E^1_k \ast E^2_k$. Kao and Hwang [17] highlighted the problem of non-unique optimal multipliers solved from (1); they give a solution based on the set of multipliers which provide the largest $E^1_k$ while keeping the total efficiency score at $E_k$ derived from (1) for the objective

$$
E^1_k = \max \left( \sum_{p=1}^{q} w_p Z_{pk} \right) \quad \text{s.t.} \quad \sum_{i=1}^{m} v_i X_{ik} = 1
$$

$\sum_{i=1}^{m} v_i X_{ik} = 1$, by adding one more constraint

$$
\sum_{r=1}^{s} u_r Y_{rk} - E_k \sum_{i=1}^{m} v_i X_{ik} = 0
$$

and keeping all the other constraints in (1). After $E^1_k$ is calculated, the efficiency of the second stage is obtained as:

$$
E^2_k = E_k / E^1_k.
$$

General two-stage DEA

The general two-stage network DEA model of Kao [16] gives more freedom to alter the internal structure of the production process before achieving the final output. It differs from the basic two-stage network DEA model of Kao and Hwang [17] in terms of additional outputs and input measures. The production process is as follows: (1) inputs of stage 1 produce exogenous outputs (undesirable outputs) and intermediate products (desirable outputs), (2) dropping of undesirable outputs produced in stage 1 while carrying forward the desirable outputs along with additional inputs$^2$ into stage 2, (3) this produces final outputs in stage 2.

The general two-stage network DEA model is given as the following linear program:

$$
E_0 = \max \left( \sum_{r=1}^{s} u_r Y_{r0} \right) \quad \text{s.t.} \quad \sum_{i=1}^{m} v_i X_{i0} = 1
$$

$$
\sum_{r=1}^{s} u_r Y_{rj} - \sum_{g=1}^{h} W_g Z_{gj} - \sum_{i=1}^{m} V_i X_{ij} \leq 0, \quad j = 1 \ldots n
$$

$$
\sum_{r=1}^{s} u_r Y_{rj} - \sum_{g=1}^{h} W_g Z_{gj} \leq 0, \quad j = 1 \ldots n
$$

$$
u_r, V_i, W_g \geq 0, \quad r = 1 \ldots s, \quad i = 1 \ldots m, \quad g = 1 \ldots h
$$

(2)

For expressing simply, we removed the non-Archimedean number $e$. At optimality, the system and division efficiencies are calculated as:

$$
E_k^e = \sum_{r=1}^{s} u_r Y_{r0}^{\text{undesirable}} + \sum_{r=1}^{s} u_r Y_{r0}^{\text{final}}
$$

$$
E^1_k = \left( \sum_{r=1}^{s} u_r Y_{r0}^{\text{undesirable}} + \sum_{g=1}^{h} W_g Z_{g0} \right) / \sum_{i=1}^{m} V_i X_{i0}
$$

$$
E^2_k = \sum_{r=1}^{s} u_r Y_{r0}^{\text{final}} / \sum_{g=1}^{h} W_g Z_{g0}
$$

Even though the intermediate products $Z_g$ are not reflected directly in calculating the system efficiency $E_k^e$, they have been considered for in deriving the division efficiencies $E^1_k$ and $E^2_k$ which will affect $E_k^e$ through the multiplier $U_r$ and $V_i$. For decomposing the system efficiency into divisional efficiencies done through the following equation

$$
E_k^e = \omega^1 E_k^e + \omega^2 E_k^e
$$

where

$$
\omega^1 = \sum_{i=1}^{m} V_i X_{i0} / \sum_{i=1}^{m} V_i X_{i0} + \sum_{r=1}^{s} u_r Y_{r0}^{\text{undesirable}}
$$

$$
\omega^2 = \sum_{g=1}^{h} W_g Z_{g0} + V_i X_{i0} / \left( \sum_{i=1}^{m} V_i X_{i0} + \sum_{r=1}^{s} u_r Y_{r0}^{\text{undesirable}} \right)
$$

Data

We used data from 46 banks of India (26 public sector banks, 20 private sector banks) for the period from 2014 to 2016, mainly collected from the Statistical Tables Relating to Banks in India published by the Reserve Bank of India (www.rbi.org.in). These 46 banks represent more than 85% of banking business across India. Also, there are 43 foreign and 51 cooperative banks that hold less than 15% of the banking business. Therefore, we are not included foreign banks and cooperative banks in our analysis. The shareholding pattern of these banks was collected from the latest Annual Reports of the respective banks to corroborate any effects on the efficiency gap. For the analysis, we applied the same definitions and variables used by Gulati and Kumar [13], Kumar and Gulati [18] and Sharma and Dalip [25]. For the standard

$^2$ In this study no new additional input is introduced in the stage 2.
two-stage network DEA, we considered fixed assets ($x_1$), employees ($x_2$), and loanable funds ($x_3$) (deposits plus borrowings) as inputs along with advances ($z_1$) and investments ($z_2$) as intermediaries and net interest income ($y_1$) and non-interest income ($y_2$) as final outputs. For the general two-stage network DEA, we separated net NPA ($y^{\text{undesirable}}$) from the advances ($z_1$) and used it as an undesirable output in the model with the rest of the advances ($z_1^*$) modeled as an intermediary along with investments ($z_2$). Figure 1 gives the flowchart of the general two-stage DEA.

**Result and discussions**

Table 1 provides the system and divisional efficiency scores from both the standard and the general two-stage network DEA models for the 46 banks with a constant return to scale (CRS) for the year 2016. From the standard two-stage model, there exists, on average, a 40.7% inefficiency in the banking sector of India with system efficiency score ranging from 0.325 to 1. On average, stage 2 efficiency is lesser than the stage 1 efficiency score indicates these banks are relatively efficient in collecting deposits compared to the effective management of loans and advances. The overall performance of all the banks distinctly improves in the general two-stage model where NPAs are used as an exogenous output from the first stage, reducing the inefficiency to 24.4% with the system efficiency score ranging from 0.527 to 1.

Further, the results show that, on average, around 16.2% of efficiency loss in the Indian banking system is contributed by the NPAs. Thus, the banks can improve their efficiency by managing the level of NPAs, indicating that the cost of NPAs includes not only the cost of actual NPAs and its interest earnings but also the cost associated with the efficiency loss. For robustness, we also estimated the efficiency gap for the data of the years 2014 and 2015 and found that the average efficiency gap due to NPAs was 12.8 and 13.6 percentage, respectively, indicating an increase in the average efficiency gap over the years which is a characteristic of the frequent failure of banking policies about NPAs.

The average efficiency gap due to NPAs in 2016 for the public sector banks (first 26 banks in Table 1), which dominate the Indian banking system in terms of the size, is 25.6%. This is very high compared to the overall efficiency gap as well as the average efficiency gap of the private banks (last 20 banks in Table 1) that stood at 4%. We also examined this for the years 2014 and 2015; the results are presented in Table 2. The results show the efficiency gap is increasing over the years as it stands at 12.9, 13.2, and 16.2% for the years 2014, 2015, and 2016, respectively, indicating the growing problem of NPAs in the Indian banking system. Further, we can observe that the efficiency gap for public sector banks is higher for the years 2014 and 2015.

Since the public sector banks have a higher efficiency gap, we also compared the relationship between the shareholding structure and the efficiency gap to understand the performance of the banks concerning the shareholding pattern. There are four shareholder groups in the Indian banking system, viz. government, institutions, public, and private. The correlation between the shareholding percentages of each of these groups and the efficiency gap is calculated and presented in Table 3. The results indicate a positive correlation between the efficiency gap and the government shareholdings, whereas institutional, public, and private shareholdings are negatively correlated with the efficiency gap. This clearly suggests that the banks with higher public shareholdings have lower levels of efficiency gap (due to NPAs) as compared to the banks which have more government or private shareholding. The situation could be further
| Name of the bank                               | Standard two-stage DEA | General two-stage DEA | Efficiency gap |
|------------------------------------------------|------------------------|-----------------------|----------------|
|                                                | Stage 1 Efficiency score | Stage 2 Efficiency score | System Efficiency score |
|                                                |                          |                        |                          |
| State Bank of Bikaner & Jaipur                 | 1.000                   | 0.751                 | 0.751                    | 1.000                   | 0.785 | 0.885 | 0.134 |
| State Bank of Hyderabad                         | 1.000                   | 0.692                 | 0.692                    | 0.982                   | 0.694 | 0.847 | 0.155 |
| State Bank of India                             | 1.000                   | 0.689                 | 0.689                    | 0.946                   | 0.712 | 0.805 | 0.116 |
| State Bank of Mysore                            | 0.885                   | 0.658                 | 0.583                    | 0.929                   | 0.685 | 0.681 | 0.098 |
| State Bank of Patiala                           | 0.884                   | 0.548                 | 0.484                    | 0.922                   | 0.568 | 0.888 | 0.404 |
| State Bank of Travancore                        | 0.886                   | 0.645                 | 0.572                    | 0.807                   | 0.693 | 0.683 | 0.112 |
| Allahabad Bank                                  | 0.869                   | 0.633                 | 0.550                    | 0.976                   | 0.676 | 0.732 | 0.182 |
| Andhra Bank                                     | 0.922                   | 0.659                 | 0.607                    | 0.971                   | 0.679 | 0.716 | 0.109 |
| Bank of Baroda                                  | 0.786                   | 0.560                 | 0.440                    | 0.746                   | 0.588 | 0.654 | 0.214 |
| Bank of India                                   | 0.782                   | 0.531                 | 0.415                    | 0.870                   | ∞      | 0.870 | 0.455 |
| Bank of Maharashtra                             | 0.845                   | 0.610                 | 0.516                    | 0.913                   | 0.609 | 0.823 | 0.307 |
| Canara Bank                                     | 0.787                   | 0.533                 | 0.419                    | 0.696                   | 0.568 | 0.621 | 0.201 |
| Central Bank of India                           | 0.803                   | 0.628                 | 0.504                    | 0.916                   | 0.673 | 0.691 | 0.187 |
| Corporation Bank                                | 0.903                   | 0.513                 | 0.463                    | 1.000                   | ∞      | 1.000 | 0.537 |
| Dena Bank                                       | 0.823                   | 0.485                 | 0.399                    | 0.639                   | ∞      | 0.639 | 0.240 |
| IDBI Bank Limited                               | 0.791                   | 0.514                 | 0.406                    | 1.000                   | ∞      | 1.000 | 0.594 |
| Indian Bank                                     | 0.872                   | 0.583                 | 0.508                    | 0.915                   | 0.607 | 0.610 | 0.102 |
| Indian Overseas Bank                            | 0.785                   | 0.585                 | 0.459                    | 1.000                   | ∞      | 1.000 | 0.541 |
| Oriental Bank of Commerce                       | 0.853                   | 0.592                 | 0.505                    | 0.865                   | 0.631 | 0.788 | 0.283 |
| Punjab and Sind Bank                            | 0.831                   | 0.544                 | 0.452                    | 0.883                   | 0.552 | 0.557 | 0.105 |
| Punjab National Bank                            | 0.848                   | 0.643                 | 0.546                    | 1.000                   | ∞      | 1.000 | 0.454 |
| Syndicate Bank                                  | 0.885                   | 0.507                 | 0.449                    | 0.892                   | 0.530 | 0.570 | 0.121 |
| UCO Bank                                        | 0.689                   | 0.631                 | 0.435                    | 0.758                   | ∞      | 0.758 | 0.323 |
| Union Bank of India                             | 0.888                   | 0.535                 | 0.476                    | 0.784                   | 0.563 | 0.684 | 0.209 |
| United Bank of India                            | 0.710                   | 0.633                 | 0.449                    | 0.793                   | ∞      | 0.793 | 0.344 |
| Vijaya Bank                                     | 0.821                   | 0.506                 | 0.415                    | 0.791                   | 0.529 | 0.546 | 0.131 |
| Axis Bank                                       | 0.941                   | 0.903                 | 0.850                    | 0.946                   | 0.907 | 0.858 | 0.008 |
| Catholic Syrian Bank Ltd                        | 0.666                   | 0.674                 | 0.449                    | 0.703                   | 0.702 | 0.527 | 0.078 |
| City Union Bank Limited                         | 0.978                   | 0.795                 | 0.777                    | 0.979                   | 0.805 | 0.792 | 0.015 |
| DCB Bank Limited                                | 0.987                   | 0.795                 | 0.785                    | 1.000                   | 0.800 | 0.800 | 0.014 |
| Dhanlaxmi Bank                                  | 0.785                   | 0.653                 | 0.513                    | 0.742                   | 0.708 | 0.548 | 0.035 |
| Federal Bank                                    | 0.926                   | 0.711                 | 0.658                    | 0.928                   | 0.717 | 0.670 | 0.012 |
| HDFC Bank                                       | 1.000                   | 1.000                 | 1.000                    | 1.000                   | 1.000 | 1.000 | 0.000 |
| ICICI Bank                                      | 0.897                   | 0.951                 | 0.853                    | 0.909                   | 0.977 | 0.891 | 0.038 |
| IDFC Bank                                       | 1.000                   | 0.325                 | 0.325                    | 0.976                   | 0.332 | 0.669 | 0.344 |
| Indusind Bank                                   | 0.951                   | 1.000                 | 0.951                    | 0.968                   | 1.000 | 0.968 | 0.017 |
| Jammu & Kashmir Bank Ltd                        | 0.859                   | 0.878                 | 0.754                    | 0.902                   | 0.903 | 0.827 | 0.073 |
| Karnataka Bank Ltd                              | 0.846                   | 0.655                 | 0.555                    | 0.833                   | 0.669 | 0.583 | 0.028 |
| Karur Vysya Bank                                | 0.957                   | 0.770                 | 0.737                    | 0.963                   | 0.772 | 0.744 | 0.007 |
| Kotak Mahindra Bank Ltd                         | 0.929                   | 0.974                 | 0.905                    | 0.935                   | 0.982 | 0.918 | 0.013 |
| Lakshmi Vilas Bank                              | 0.923                   | 0.575                 | 0.530                    | 0.931                   | 0.580 | 0.542 | 0.011 |
| Nainital Bank                                   | 0.745                   | 1.000                 | 0.745                    | 0.776                   | 1.000 | 0.776 | 0.031 |
| RBL                                             | 0.843                   | 0.692                 | 0.583                    | 0.833                   | 0.717 | 0.597 | 0.014 |
| South Indian Bank                               | 0.894                   | 0.606                 | 0.542                    | 0.898                   | 0.621 | 0.596 | 0.054 |
| Tamilnadu Mercantile Bank Ltd                   | 0.980                   | 0.758                 | 0.742                    | 0.981                   | 0.759 | 0.748 | 0.005 |
| Yes Bank Ltd.                                   | 1.000                   | 0.859                 | 0.859                    | 1.000                   | 0.859 | 0.862 | 0.003 |
| Average                                         | 0.875                   | 0.674                 | 0.593                    | 0.896                   | 0.715 | 0.756 | 0.162 |

* ∞ — scores not calculated by the model
### Table 2 Efficiency scores and efficiency gap

| Name of the bank                          | 2014 Efficiency score | Efficiency score* | Efficiency gap | 2015 Efficiency score | Efficiency score* | Efficiency gap |
|------------------------------------------|-----------------------|-------------------|----------------|-----------------------|-------------------|----------------|
| State Bank of Bikaner & Jaipur           | 0.728                 | 0.945             | 0.217          | 0.694                 | 0.746             | 0.052          |
| State Bank of Hyderabad                  | 0.648                 | 0.847             | 0.199          | 0.692                 | 0.719             | 0.027          |
| State Bank of India                      | 0.636                 | 0.674             | 0.038          | 0.677                 | 0.694             | 0.017          |
| State Bank of Mysore                     | 0.571                 | 0.667             | 0.096          | 0.625                 | 0.644             | 0.019          |
| State Bank of Patiala                    | 0.522                 | 0.911             | 0.388          | 0.546                 | 1.000             | 0.454          |
| State Bank of Travancore                 | 0.513                 | 0.831             | 0.319          | 0.518                 | 0.557             | 0.039          |
| Allahabad Bank                           | 0.549                 | 0.859             | 0.311          | 0.653                 | 0.888             | 0.235          |
| Andhra Bank                              | 0.508                 | 1.000             | 0.492          | 0.586                 | 0.650             | 0.064          |
| Bank of Baroda                           | 0.417                 | 0.511             | 0.094          | 0.483                 | 0.592             | 0.108          |
| Bank of India                            | 0.432                 | 0.593             | 0.160          | 0.456                 | 0.911             | 0.455          |
| Bank of Maharashtra                      | 0.569                 | 0.385             | 0.016          | 0.646                 | 0.934             | 0.288          |
| Canara Bank                              | 0.431                 | 0.473             | 0.042          | 0.429                 | 0.521             | 0.092          |
| Central Bank of India                    | 0.494                 | 1.000             | 0.506          | 0.555                 | 0.651             | 0.096          |
| Corporation Bank                         | 0.422                 | 1.000             | 0.578          | 0.463                 | 1.000             | 0.537          |
| Dena Bank                                | 0.441                 | 0.505             | 0.063          | 0.452                 | 0.717             | 0.266          |
| Idbi Bank Limited                        | 0.497                 | 1.000             | 0.503          | 0.533                 | 1.000             | 0.467          |
| Indian Bank                              | 0.529                 | 0.569             | 0.040          | 0.570                 | 0.591             | 0.021          |
| Indian Overseas Bank                     | 0.453                 | 0.664             | 0.211          | 0.446                 | 1.000             | 0.554          |
| Oriental Bank of Commerce                | 0.526                 | 0.731             | 0.205          | 0.543                 | 0.815             | 0.273          |
| Punjab and Sind Bank                     | 0.380                 | 0.755             | 0.375          | 0.417                 | 0.788             | 0.370          |
| Punjab National Bank                     | 0.658                 | 0.687             | 0.029          | 0.660                 | 0.861             | 0.201          |
| Syndicate Bank                           | 0.491                 | 0.501             | 0.010          | 0.436                 | 0.474             | 0.038          |
| UCO Bank                                 | 0.568                 | 0.639             | 0.071          | 0.551                 | 1.000             | 0.449          |
| Union Bank of India                      | 0.492                 | 0.570             | 0.078          | 0.536                 | 0.647             | 0.111          |
| United Bank of India                     | 0.484                 | 1.000             | 0.516          | 0.563                 | 1.000             | 0.437          |
| Vijaya Bank                              | 0.337                 | 0.425             | 0.088          | 0.384                 | 0.473             | 0.089          |
| Axis Bank                                | 0.900                 | 0.900             | 0.000          | 0.854                 | 0.854             | 0.000          |
| Catholic Syrian Bank Ltd                 | 0.523                 | 0.550             | 0.027          | 0.509                 | 0.676             | 0.167          |
| City Union Bank Limited                  | 0.679                 | 0.682             | 0.003          | 0.712                 | 0.722             | 0.010          |
| DCB Bank Limited                         | 0.637                 | 0.643             | 0.006          | 0.760                 | 0.768             | 0.008          |
| Dhanlaxmi Bank                           | 0.410                 | 0.357             | 0.147          | 0.473                 | 0.526             | 0.053          |
| Federal Bank                             | 0.686                 | 0.686             | 0.000          | 0.697                 | 0.699             | 0.002          |
| HDFC Bank                                | 0.955                 | 0.955             | 0.000          | 0.965                 | 0.965             | 0.000          |
| ICICI Bank                               | 0.846                 | 0.846             | 0.000          | 0.873                 | 0.873             | 0.000          |
| IDFC Bank                                | 0.765                 | 0.765             | 0.000          | 0.751                 | 0.752             | 0.001          |
| Indusind Bank                            | 0.961                 | 0.961             | 0.000          | 0.946                 | 0.946             | 0.000          |
| Jammu & Kashmir Bank Ltd                 | 0.763                 | 0.763             | 0.000          | 0.841                 | 0.858             | 0.017          |
| Karnataka Bank Ltd                       | 0.554                 | 0.563             | 0.010          | 0.531                 | 0.551             | 0.020          |
| Karur Vysya Bank                         | 0.578                 | 0.578             | 0.000          | 0.658                 | 0.658             | 0.000          |
| Kotak Mahindra Bank Ltd                  | 1.000                 | 1.000             | 0.000          | 1.000                 | 1.000             | 0.000          |
| Lakshmi Vilas Bank                       | 0.529                 | 0.630             | 0.101          | 0.525                 | 0.539             | 0.015          |
| Nainital Bank                            | 0.723                 | 0.723             | 0.000          | 0.712                 | 0.723             | 0.011          |
| RBL                                      | 0.648                 | 0.648             | 0.000          | 0.599                 | 0.599             | 0.000          |
| South Indian Bank                        | 0.561                 | 0.561             | 0.000          | 0.544                 | 0.545             | 0.001          |
| Tamilnad Mercantile Bank Ltd             | 0.783                 | 0.785             | 0.002          | 0.739                 | 0.742             | 0.003          |
| Yes Bank Ltd                             | 0.774                 | 0.774             | 0.000          | 0.749                 | 0.749             | 0.000          |
| Average                                  | 0.599                 | 0.729             | 0.129          | 0.621                 | 0.753             | 0.132          |

* Efficiency score from General two stage DEA model
This massive, weighed down by NPAs of the public sector banks forced the government to initiate action toward resolving the situation. The Government of India recently decided to inject Rs. 2.1 trillion through various channels as a measure to recapitalize these public sector banks. In order to see whether this recapitalization measure will bridge the efficiency gap, we ran a separate general two-stage network DEA with capital injection as an exogenous input entering in stage 2 of the model. Since the actual level of the capital injection is not known at present, we calculated 15 and 25% of the gross NPAs as a capital injection for each bank and found a reduction in the efficiency gap.3 The main policy implication from this analysis is that efficiency could be achieved by reducing the government’s shareholding in these banks. Further, recapitalization helps the banks to reduce the adverse effects of NPAs.

**Conclusion**

This study aims to understand the extent of inefficiency in the Indian banking sector due to non-performing assets (NPAs) using data on 46 banks for the financial year 2016. The analysis was carried out in an intermediation approach to understand the divisional and system efficiency of the banks, first with the standard two-stage network DEA model of Kao and Hwang [17] and then with the general two-stage network DEA model of Kao [16] by keeping NPAs as an undesirable exogenous output to understand the efficiency gap due to NPAs. The efficiency estimates of these two models have shown that around 16.2% of the efficiency loss arises due to NPAs in the Indian banking sector.

This highlights the fact that NPAs are squeezing banks’ capital position and profitability, leading to further deterioration of the Indian banking sector and the economy. Also, the analysis has shown that the shareholding pattern affected the efficiency gap. The results revealed that the banks with more public shareholding have a lower level of efficiency gap due to NPAs as compared to those which have more government or private shareholding. The managerial implications derived from this study are twofold: First, the banks can improve their efficiency by managing the level of NPAs. Second, it indicates that the cost of NPAs includes not only the cost of actual NPAs and its interest earnings but also the cost associated with the efficiency loss. Further, the findings also suggest that in addition to recapitalizing the public sector banks, disinvesting the government shareholding could improve the efficiency of these banks.

**Abbreviations**

NPA: non-performing assets; DEA: data envelopment analysis; CRS: constant return to scale; DMU: decision making units; RBI: Reserve Bank of India.

**Acknowledgements**

The authors thank the editor and two anonymous referees of this journal for their valuable comments on this paper.

**Authors’ contributions**

All the authors HK, AS, and RSD have equal contributions in conceiving the idea and analyzing the empirical results. HK and AS prepared the introduction, literature review, and collected data for the study. RSD contributed in estimating the model. All authors have read and approved the manuscript.

**Funding**

The authors declare that no funding from any agencies was received for this study.

**Availability of data and materials**

The data used in this paper are collected from the Reserve Bank of India database (RBI) (www.rbi.org.in).

**Competing interests**

The authors declare that they have no competing interests.

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Received: 22 July 2019   Accepted: 5 May 2020

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3 The results of this analysis are not presented here but can be obtained from the authors upon request.
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