Multi-Criteria Optimization of a Biomass-Based Hydrogen Production System Integrated With Organic Rankine Cycle

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Biomass-based gasification is an attractive and promising pathway for hydrogen production. In this work, a biomass-based hydrogen production system integrated with organic Rankine cycle was designed and investigated to predict the performance of hydrogen production yield and electricity generation under various operating conditions. The modified equilibrium model presented desirable results for the produced syngas compositions compared with the experimental data. Hydrogen yields from four types of biomass (wood chips, daily manure, sorghum, and grapevine pruning wastes) were compared under the same operating condition, with wood chips exhibiting the maximum hydrogen yield of 11.59 mol/kg. The effects of gasification temperature, equivalence ratio, and steam-to-biomass ratio on the hydrogen yield and electricity generation were investigated by using the response surface method. Furthermore, the system was optimized using a genetic algorithm based on the response surface model. A preferred optimal solution with a hydrogen yield of 39.31 mol/kg and an output power of 3,558.08 kW (0.99 kW h/kg) was selected by the linear programming technique for multidimensional analysis of the preference method.

Keywords: biomass gasification, non-equilibrium model, hydrogen production, response surface method, multi-objective optimization

INTRODUCTION

Hydrogen is one of the promising energy sources and will be most likely to play a critical role in energy production, energy storage, and transport sector in the future (Salam et al., 2013). Currently, hydrogen is dominantly produced from fossil energy, specifically natural gas. Renewable sources such as solar and biomass can be utilized to produce hydrogen through various production pathways including electrolysis, photo-electrochemical, and thermochemical processes (Puigarnavat et al., 2010). Biomass gasification as an alternative pathway has received substantial attention for hydrogen-rich syngas and enhanced hydrogen production in the past two decades due to its high energy efficiency and low CO₂ emissions (Li et al., 2001). Biomass feedstocks such as agricultural and forestry residues, dedicated energy crops, and industrial and municipal wastes are potential energy sources and suitable for hydrogen production (Salam et al., 2018).

Over the past years, many studies have been carried out to predict the optimal operating conditions and system performance based on different models of biomass gasification (Wang and Kinoshita, 1992; Gil et al., 1997; Chen et al., 2016). Modeling methods for gasification include...
equilibrium models (Watkinson et al., 1991), kinetic models, dynamic models for specific reactor types, and neural network models (Inayat et al., 2020). The equilibrium model is usually based on the principle of Gibbs free energy minimization. The kinetic model requires a clearly defined kinetic reaction mechanism. For more complex systems, the reaction mechanism requires extensive and detailed reaction information (Vamvuka et al., 1995). The dynamic model provides relatively complete information about the reaction mechanism and reactor configuration, while thermodynamic equilibrium calculations are independent of the gasifier type, and the model is more suitable for process design studies on the influence of the fuels and process parameters (Karmakar and Datta, 2011).

Zainal et al. (2001) established the gasification model of wood chips based on the equilibrium model and verified the reliability of the equilibrium model through experimental data. The hydrogen volume fraction (20–25%) increased with the increasing moisture content in the wood chips. Couto et al. (2015) evaluated and compared the performance of the equilibrium model based on Gibbs free energy minimization and the CFD method in semi-industrial-scale fluidized bed gasification modeling. The results showed that the established equilibrium model can effectively predict the product syngas composition using different raw materials under different operating conditions. The CFD model provided dynamic information and can estimate the composition of syngas or other operating parameters at any point in time and space. The equilibrium model based on Gibbs free energy minimization was desirable by comparing the prediction results. Arun et al. (2016) used an equilibrium model to calculate and determine the effects of the equivalence ratio (ER), moisture content (MC), and reaction temperature (RT) on corn cob gasification in the down draft gasifier. They found from the simulation results that when the equivalence ratio was greater than 0.3, the composition of hydrogen and carbon monoxide predicted by the model was close to the experimental values.

In recent years, some scholars have modified the biomass gasification equilibrium model through actual experimental data for better prediction of syngas composition. Kaewluan and Pipatmanomai (2011) measured the carbon conversion efficiency (79–87%) of wood chips during bubbling fluidized bed gasification. The carbon conversion efficiency increased with the increasing gasification temperature. Lapuerta et al. (2008) conducted experiments on different biomass wastes including grapevine pruning wastes, pinus pruning, and sawdust. They determined different carbon conversion efficiencies (50–98%) under different operating conditions. Both equivalence ratio and gasification temperature gave a positive effect on the carbon conversion efficiency. Rodriguez-Alejandro et al. (2016) also discussed adjusting the equilibrium constants of the methanation reaction and water–gas shift reaction to modify the ratio of methane and carbon monoxide in syngas production.

Since the syngas at the outlet of the gasifier contains high enthalpy, it is necessary to recover and utilize this energy to improve the system efficiency. The organic Rankine cycle, another important subsystem involved in this study, is one of the best candidates to recover waste heat from energy systems into power due to its reliability, easy maintenance, and economic feasibility (Yu et al., 2017). Behzadi et al. (2020) proposed a biomass-fired proton exchange membrane fuel cell (PEMFC) integrated with an organic Rankine cycle and thermoelectric generator using different gasification agents. The results revealed that steam as the gasification agent is more suitable in terms of the economic and environmental performance indicators. Results of multi-objective optimization indicated that the output power and total cost rate using steam as the gasification agent are 1.849 kW and 5.094 $/h, respectively. A heat recovery system was employed for power generation from a PEM fuel cell’s waste heat by Marandi et al. (2019). The proposed system which involved the parallel organic Rankine cycle for utilizing the provided heat could generate 1,353 kW power. Energy efficiency and exergy efficiency of the overall system were computed to be 58.15 and 36.64%, respectively.

As for hydrogen or hydrogen-rich syngas production from biomass gasification, most studies focused on improving the hydrogen yield and integrating the gasification process with a hydrogen PEM fuel cell or solid oxide fuel cell for downstream processing, while how to make good use of the waste heat from the processes lacks investigation. Therefore, in this work, we proposed a designed system of enhanced hydrogen production from biomass gasification with waste heat recovery for electricity generation from the organic Rankine cycle. Based on the designed system, the optimal product yields and corresponding operational conditions were analyzed and identified using a set of mathematical methods. The overall analysis was organized through the following steps. At first, the equilibrium model, which is frequently used and generally exhibited a large deviation in syngas compositions, was modified by accounting for carbon conversion efficiency and equilibrium constant correction to reflect a solid validation and prediction of the system performance. On the basis of the process model, a regression model was subsequently established and the response surface methodology was applied to predict the optimal hydrogen yield and output power from the system for multi-generation purposes. By taking advantage of the constructed regression model, the multi-objective optimization method was introduced to project the optimal state points of the system under various conditions. This application could shed light on how to improve the system design and its overall performance in terms of specific indicators.

**Materials and Methods**

**System Description**

The proximate and ultimate compositions of the feedstock including wood chips, daily manure, sorghum, and grapevine (Lapuerta et al., 2008; Huang, 2009; Maglino et al., 2015; Rodriguez-Alejandro et al., 2016) are presented in Table 1. Among the four biomass, the hydrogen contents of wood chips and sorghum are higher, while daily manure owns the
lowest volatile content and hydrogen content. The simplified flow diagram of the designed system for producing hydrogen and electricity is shown in Figure 1. The system consists of five main units: the 1) biomass gasification unit, 2) steam methane reforming unit (SMR), 3) water–gas shift unit (HTS and LTS), 4) hydrogen separation unit (PSA), and 5) organic Rankine cycle (ORC). The key parameters and main assumptions associated with these modules are listed in Table 2, and the thermodynamic calculations and the system evaluation are performed using Python.

**Gasification Unit**

Table 3 presents the most common chemical reactions (Basu, 2013; Molino et al., 2016) employed by equilibrium models. The Boudouard reaction, char reforming reaction (or water–gas reaction), water–gas shift, and methane formation are widely used as indicated in the literature, while the methane reforming reaction is also considered in some articles (Dupont et al., 2007; Jarunthammachote and Dutta, 2007; Melgar et al., 2007; Azzone et al., 2012; Couto et al., 2013; Dutta et al., 2014; La Villetta et al., 2017; Susastriawan et al., 2017; Shayan et al., 2018). In this work, the following four reactions were used to describe the gasification reaction, as shown in Eqs 1–4:

\[
\text{Boudouard reaction : } C + CO_2 \leftrightarrow 2CO \tag{1} \\
\text{Char reforming reaction : } C + H_2O \leftrightarrow CO + H_2 \tag{2} \\
\text{Water–gas shift reaction : } CO + H_2O \leftrightarrow CO_2 + H_2 \tag{3} \\
\text{Methane formation reaction : } C + 2H_2 \leftrightarrow CH_4 \tag{4}
\]

The equilibrium constants for the methane formation reaction and water–gas shift reaction are shown in Eqs 5 and 6, where \( P_i \) and \( X_i \) are the partial pressure and molar yield of the specific gas, respectively. The equilibrium constant \( K \) can be calculated using Eq. 7, where \( R \) is the ideal gas constant and \( T \) refers to the gasification temperature. The Gibbs function (\( \Delta G \)) is defined in Eq. 8, where \( g_i \) is the specific Gibbs free energy formation and \( v_i \) is the reaction rate for each species. Equation 9 shows the Gibbs free energy for a singular species from the JANAF

![Flow diagram of the biomass-based hydrogen production system.](image-url)
The gasification process is assumed to be adiabatic; thus, the heat balance can be derived according to Eq. 14 as indicated by Zainal et al. (2001):
\[
dH_{biomass} + (w + w_{steam})dH_{H_2O(l)} = x_1dH_{H_2} + x_2dH_{CO} + x_3dH_{CO_2} + x_4dH_{H_2O(vap)} + x_5dH_{CH_4} + 3.76m_{air}dH_N_2
\]  
(14)
where \(dH_{gas}\) is the sum of heat formation and enthalpy change.
\[
dH_{gas} = H_0^f + \Delta H = H_0^f + \Delta T(C_{p(gas)})
\]
\[
dH_{H_2O(l)} = H_0^f + H_{H_2O(vap)}
\]
\[
dH_{biomass} = H_0^f + H_{biomass}
\]
where \(C_{p(gas)}\) is the specific heat of the gas and \(H_{(vap)}\) is the latent heat of evaporation.

To solve the unknown gas species concentrations, the equation set including Eqs 5 and 6 and 11–14 is closed and solved simultaneously by using the Newton–Jacobi method using Python.

**Steam Methane Reforming Unit**
The syngas from the gasifier is fed into the steam methane reforming (SMR) unit to enhance the hydrogen production from methane. The steam methane reforming reaction is endothermic and tends to shift to the right side at high temperatures. For simplification, the operating temperature of the SMR system is set to be consistent with the gasifier, and the reactor is recovered through heat exchanges via the organic Rankine cycle (ORC).

**Water–Gas Shift Unit**
A two-step water–gas shift reaction is adopted in the system to enhance the hydrogen production from carbon monoxide conversion. Two WGS reactors with one at a high temperature (HTS) of 673 K and the other at a low temperature (LTS) of 473 K are employed in the system (Moneti et al., 2016). Excess heat from the reactor is recovered through heat exchanges via the organic Rankine cycle (ORC).

**Separation Unit**
The pressure swing adsorption (PSA) unit is required to gain high hydrogen purity. Pressurization is achieved by a compressor before the PSA. A separation efficiency of 70% for hydrogen

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**TABLE 2** | Input operating parameters (Marandi et al., 2019; Behzadi et al., 2020).

| Parameter | Value |
|-----------|-------|
| Gasifier  | —     |
| Biomass mass flow rate (kg/s) | 1     |
| Operating pressure (bar) | 1     |
| Air inlet temperature (K) | 298   |
| Moisture content (%) | 10    |
| SMR       | —     |
| Operating pressure (bar) | 1     |
| Steam-to-carbon ratio | 1     |
| HTS        | —     |
| Operating temperature (K) | 673   |
| Operating pressure (bar) | 1     |
| PSAD      | —     |
| Operating pressure (bar) | 7     |
| Efficiency (%) | 70    |
| ORC       | —     |
| Pump outlet pressure (bar) | 25    |
| Turbine outlet temperature (K) | 250   |
| Condenser outlet temperature (K) | 230   |
| Pump efficiency (%) | 90    |
| Turbine efficiency (%) | 85    |

SMR, steam methane reforming unit; HTS, high temperature shift reactor; LTS, low temperature shift reactor; ORC, organic Rankine cycle; WGS, water–gas shift reactor; PSA, pressure swing adsorption unit.

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The thermochemical tables and the values of constants from Agi to Ggi are referenced in Supplementary Table S1 (Turns, 2000).

\[
K_1 = \frac{P_{CH_4}}{(P_{H_2})^2} = \frac{X_{CH_4}}{X_{H_2}} \quad (5)
\]
\[
K_2 = \frac{P_{CO}P_{H_2}}{P_{COH_2}P_{H_2O}} = \frac{X_{CO}X_{H_2}}{X_{COH_2}X_{H_2O}} \quad (6)
\]
\[
\ln K = \frac{\Delta G}{RT} \quad (7)
\]
\[
\frac{\Delta G}{RT} = \sum v_{fgi}(T) \quad (8)
\]
\[
g_i(T) = A_{gi} + B_{gi}T + C_{gi}T^2 + D_{gi}T^3 + E_{gi}T^4 + \frac{F_{gi}}{T} + G_{gi}lnT \quad (9)
\]

In all cases, sulfur and nitrogen contents were ignored due to the low S and N contents in biomass. The global gasification reaction can be written as follows:
\[
CH_4O_y + wH_2O + w_{steam}H_2O + m_{air}O_2 + 3.76m_{air}N_2 = x_1H_2 + x_2CO + x_3CO_2 + x_4H_2O + x_5CH_4 + 3.76m_{air}N_2 \quad (10)
\]
where \(x\) and \(y\) are the number of atoms of hydrogen and oxygen per number of atom of carbon in the biomass, \(w\) is the mole of moisture per mol of biomass, \(w_{steam}\) is the mole of steam added per mol of dry ash–free biomass, \(m_{air}\) is the mole of oxygen per mol of biomass, and \(x_i\) is the molar number of the unknown product gas. Elemental balances of carbon, oxygen, and hydrogen are illustrated in Eqs 11–13, respectively.

\[
x + 2w + 2w_{steam} = 2x_1 + 2x_4 + 4x_5 \quad (13)
\]

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**TABLE 3** | Reactions involved in the equilibrium model.

| Reaction (Molino et al., 2016) | — | \(\Delta H~(kJ/mol)\) (Basu, 2019) |
|-----------------------------|---|--------------------------|
| C + CO_2 ↔ 2CO               |   | +172                    |
| C + H_2O ↔ CO + H_2         |   | +131                    |
| CO + H_2O ↔ CO_2 + H_2      |   | -41.2                   |
| C + 2H_2 ↔ CH_4             |   | -74.8                   |
| CH_4 + H_2O ↔ CO + 3H_2     |   | +206                    |
and an operating pressure of 7 bar are applied in the simulation by referring to the optimized values found in the literature (Carrara et al., 2010; Villarini et al., 2016).

**ORC Unit**

In the ORC system, the organic fluid is pumped by the pump into the ORC evaporator (HX5), and subsequently, it passes through the ORC turbine to generate power. In this study, the widely used R123 with a normal boiling temperature of 300.5 K and a triple point temperature of 166 K was selected as the organic fluid (Emadi et al., 2020). Main operating parameters are shown in Table 2 referring to Marandi et al. (2019) and Behzadi et al. (2020).

As shown in Eq. 15, energy transferred to the ORC can be determined by energy conversion in Heat Exchanger 5. The generated power from the turbine and the power consumption in the pump can be calculated using Eqs 16 and 17, respectively. Due to the energy loss during the operating process, the efficiency of turbine and pump is considered to achieve the actual outlet enthalpy ($h_{28}$, $h_{30}$), as shown in Eqs 18 and 19. The enthalpy of R123 at a particular point is derived from a database called AP1700, which provides physical property data of most of the gases and refrigerants. The final calculation of the output power is calculated using Eq. 20.

$$m_{ORC} \left( h_{27} - h_{30} \right) = m_w \left( h_{25} - h_{30} \right)$$  \hspace{1cm} (15)

$$W_{\text{turbine}} = m_{ORC} \left( h_{27} - h_{28} \right)$$  \hspace{1cm} (16)

$$W_{\text{pump}} = m_{ORC} \left( h_{30} - h_{29} \right)$$  \hspace{1cm} (17)

$$\eta_{\text{turbine}} = \frac{h_{27} - h_{28}}{h_{27} - h_{28}}$$  \hspace{1cm} (18)

$$\eta_{\text{pump}} = \frac{h_{28} - h_{29, s}}{h_{29} - h_{30}}$$  \hspace{1cm} (19)

$$W_{\text{output}} = W_{\text{turbine}} - W_{\text{compressor}} - W_{\text{heater}} - W_{\text{ORC, pump}}$$  \hspace{1cm} (20)

**Model Calibration and Modification**

Thermodynamic equilibrium models usually ignore the conversion efficiency of carbon, but in fact, carbon cannot be completely converted during the gasification process (Eq. 10) (Marandi et al., 2019). Meanwhile, thermodynamic equilibriums such as the water–gas shift reaction (Eq. 3) and methanation reaction (Eq. 4) are usually hard to achieve in actual experiments. Therefore, correction factors based on experimental data were used to reflect the actual carbon conversion efficiency and nonequilibrium factors shown as follows:

$$K_{1, \text{non-eq}} = K_{1, \text{eq}} F_{X1}$$  \hspace{1cm} (21)

$$K_{2, \text{non-eq}} = K_{2, \text{eq}} F_{X2}$$  \hspace{1cm} (22)
where $K_{\text{non-eq}}$ is the modified nonequilibrium constant, $K_{\text{eq}}$ is the equilibrium constant, and $F_{K_i}$ is the correction factor of the equilibrium constants based on experimental data.

Compared with the original thermodynamic equilibrium model, correcting the equilibrium constants can improve the accuracy of hydrogen yield prediction. Besides that, $F_{K_1}$ reduces the error of methane production yield, while $F_{K_2}$ gives more accurate carbon monoxide production yield in most cases (Basu, 2013; Marandi et al., 2019; Behzadi et al., 2020). The correction factors of carbon conversion efficiency and equilibrium constant of different biomass under specific conditions are summarized in Supplementary Table S2. The RMS (root mean square) is used to compare the differences of syngas compositions between the modified model and the experimental data, as shown in Eq. 23:

$$\text{RMS} = \sqrt{\frac{\sum_{i=1}^{N} |n_{i,\text{cal}} - n_{i,\text{exp}}|^2}{N}}$$  \hspace{1cm} (23)$$

where $n_{i,\text{cal}}$ and $n_{i,\text{exp}}$ are the calculated and experimental syngas composition in vol\%, respectively, and N is the specific gas including H2, CO, and CH4.

### TABLE 4 | Average RMS values from different models.

| Biomass  | Wood chip | Sorghum |
|----------|-----------|---------|
| M1       | 2.66      | 2.85    |
| M2       | 2.20      | 2.50    |
| M3       | 1.34      | 1.75    |

RMS, root mean square.
TABLE 5 | Comparison of the average hydrogen yield.

| Volatile (wt%) | Hydrogen content in biomass (wt%) | Average hydrogen yield (mol/kg) |
|----------------|----------------------------------|--------------------------------|
| Sorghum        | 71.40                            | 6.69                           | 8.80                           |
| Manure         | 65.3                             | 5.7                            | 5.72                           |
| Wood chip      | 85.62                            | 6.62                           | 11.59                          |
| Grapevine      | 78.16                            | 5.92                           | 6.41                           |

Sensitivity Analysis and Optimization

Once establishing the full process model as aforementioned, hydrogen production and power generation can be projected according to various combinations of input operating parameters. To investigate the variation of key parameters simultaneously, the response surface methodology (RSM) was employed based on Design-Expert (DX10) version 10.0.3 software. The operating conditions of the overall system were designed by using the Box–Behnken (BBD) method, and the corresponding data were incorporated to meet the design requirements. After that, a response surface model was constructed to formulate the mathematical relationship between the target outputs such as hydrogen yields and power output and the input operational conditions, which was further illustrated by the contour plots. Therefore, the impacts of the key input parameters on the target indicator can be thoroughly explored from the sensitivity analysis.

Built upon the regression model, the multi-objective optimization of target indicators could be performed using the genetic algorithm (NSGA-II), which transforms the problem-solving process into a mechanism similar to the crossing and mutation of chromosome genes in biological evolution. The genetic algorithm was employed in this work due to its capability of speeding up the search for optimal solutions and the set of optimal solutions constituting the Pareto front and was invoked from the Geatpy platform.

RESULTS AND DISCUSSION

Model Validation

The syngas compositions from four biomass types including wood chips and sorghum were compared between different models (M1: the original equilibrium model, M2: the modified model considered the carbon conversion efficiency, and M3: the modified model considered the carbon conversion efficiency and nonequilibrium constants) and the experimental data of specific biomass. The main operating parameters (gasification temperature and equivalence ratio) of the simulation were kept consistent with the actual experimental conditions. Figure 2 shows the results of wood chip gasification under the operating conditions of gasification temperatures varying from 813 to 1,058 K and ER of 0.33. The experimental data were derived from a pilot-scale fluidized bed gasifier, and air was used as the gasification agent (Rodriguez-Alejandro et al., 2016). As shown in Figure 2A, the modified model considering carbon conversion efficiency (M2) could not improve the hydrogen production and the calculated error exceeds 100%. When both the carbon conversion efficiency and equilibrium constants were modified simultaneously (M3), the error between the predicted hydrogen production value and the experimental data was reduced to 42%. Figure 2B shows a comparison of the carbon monoxide production yield on a dry basis between different levels of models. The results of M2 were relatively close to the experimental values with a calculated error of 24.4%, while the error between M3 and the experimental values was 25.1%. Figure 2C shows a comparison of the methane production yield, and the average error was reduced by 20.9% from M3 to M1. Only when the temperature was higher than about 923 K, the predicted methane yield of theoretical models was close to the experimental data.

Figure 3 shows the results of sorghum gasification at the operating conditions of 1,013 < T < 1,073 K and ER = 0.35. The reactor was a pilot-scale fluidized bed gasifier and used air supplied by a blower as the fluidizing medium. Experimental data came from Maglinao et al. (2015). As shown in Figure 3A, the correction of the carbon conversion efficiency and the nonequilibrium constants (M3) could reduce the average error of the hydrogen production prediction values from more than 100 to 35.9% compared with the model that only modified the carbon conversion efficiency (M2). Figure 3B shows a comparison of the carbon monoxide production yield. The average error between M2 and the experimental values was reduced to 42% when the temperature was higher than about 923 K, the predicted carbon monoxide yield of theoretical models was close to the experimental data.

TABLE 6 | Thermodynamic properties for each state.

| Stream Description | T (K) | P (bar) | H (kJ) | M (kg) |
|--------------------|-------|---------|--------|--------|
| 1 Biomass (10% moisture content) | 298 | 1 | 15,192.14 | 1.07 |
| 2 Gasifier outlet inlet air | 298 | 1 | 499.42 | 1.77 |
| 3 Gasifier outlet syngas | 973 | 1 | 13,654.36 | 2.90 |
| 4 SMR outlet (hydrogen-rich) gas | 873 | 1 | 17,156.35 | 2.90 |
| 5 HX1 outlet gas | 673 | 1 | 15,672.73 | 2.90 |
| 6 HTS outlet gas | 673 | 1 | 15,322.44 | 2.94 |
| 7 HX2 outlet gas | 473 | 1 | 14,313.21 | 2.94 |
| 8 LTS outlet gas | 473 | 1 | 14,132.36 | 2.94 |
| 9 Compressor outlet gas | 591.25 | 7 | 14,801.69 | 2.94 |
| 10 PSA outlet hydrogen | 591.25 | 7 | 6,914.14 | 0.054 |
| 11 PSA outlet waste gas | 591.25 | 7 | 7,887.55 | 2.89 |
| 12 HX3 outlet hydrogen | 298 | 1 | 6,686.17 | 0.078 |
| 13 HX4 outlet waste gas | 298 | 1 | 6,615.34 | 2.89 |
| 14 Water | 298 | 1 | 142.82 | 1.37 |
| 15 Water | 298 | 1 | 54.21 | 0.52 |
| 16 Wet steam | 373 | 1 | 287.94 | 0.52 |
| 17 Dry steam | 473 | 1 | 1,386.84 | 0.52 |
| 18 Water | 298 | 1 | 88.61 | 0.86 |
| 19 Wet steam | 373 | 1 | 1,155.01 | 0.86 |
| 20 Dry steam | 673 | 1 | 2,688.63 | 0.86 |
| 21 Dry steam | 673 | 1 | 123.36 | 0.039 |
| 22 Dry steam | 673 | 1 | 1,331.66 | 0.42 |
| 23 Dry steam | 673 | 1 | 1,233.61 | 0.39 |
| 24 Gasifier outlet inlet steam | 973 | 1 | 1,579.28 | 0.39 |
| 25 Dry steam | 535.41 | 7 | 2,818.50 | 0.94 |
| 26 Water | 298 | 1 | 98.09 | 0.94 |
| 27 Organic medium | 394.56 | 1 | 3,891.45 | 12.00 |
| 28 Organic medium | 240 | 1 | 1,411.08 | 12.00 |
| 29 Organic medium | 230 | 1 | 1,158.12 | 12.00 |
| 30 Organic medium | 230 | 1 | 1,271.69 | 12.00 |
| 31 Ash | 973 | 1 | 3,016.36 | 0.29 |
48.5%, while the error between M3 and the experimental values was 21.8%. Figure 3C shows a comparison of the methane production yield. Compared with the experimental results, M2 resulted in an average error of 42.7% and the error would decrease as the temperature increased.

As shown above, the original equilibrium model (M1) overestimated the production contents of hydrogen and carbon monoxide, while the production of methane was underestimated (George et al., 2016). The errors of carbon monoxide yield prediction were reduced in M2, and M3 could effectively improve the prediction of hydrogen yield. Besides that, M3 improved the methane prediction yield of wood chips, while M2 showed higher accuracy for sorghum. RMS values gradually decreased by applying the carbon conversion efficiency and the nonequilibrium constants, as summarized in Table 4 for different biomass. In general, the modified equilibrium model is desirable for the prediction of the syngas productions of these four kinds of biomass.

Figure 4 shows the comparison of hydrogen production yield out of the gasifier between different biomass at the same operating condition of $973 < T < 1,073 \, K$ and ER of 0.3. As shown in Table 5, the trend in the hydrogen yield was as follows: wood chip (11.59 mol/kg dry biomass) > sorghum (8.80 mol/kg dry biomass) > grapevine pruning (6.41 mol/kg dry biomass) > daily manure (5.72 mol/kg dry biomass). The differences in the yields of hydrogen might be attributed to the different biomass volatiles (Wei et al., 2014; Zhang et al., 2019) or the hydrogen contents based on the ultimate analysis.

**Energy Analysis**

Different fluids were investigated to select the best working fluids for the proposed system, as illustrated in Supplementary Figure S1. Output power was used as a standard to measure the performance of the fluids. The results show that R123 is the best working fluid by generating a total power of 2,268.93 kW. Results were derived by thermodynamic modeling and considering the assumptions given in Table 6.

Furthermore, the detailed stream states of the system are shown in Sankey diagram of the energy flows (see Figure 5). The produced syngas heat is recovered to preheat the reaction agent and supplies heat to the ORC, which contributes to improving the energy conversion efficiency. Under the given design conditions, the largest energy loss occurs in the biomass gasification process since a certain proportion of biomass carbon does not react in the modified equilibrium model.

**Effects of Operating Conditions on Hydrogen Production and Output Power**

As mentioned above, wood chips produced the most maximum amount of hydrogen and showed a good degree of regression, so it was used as the biomass feedstock for further analysis. The
hydrogen production (the mole of hydrogen per kilogram of biomass, mol/kg) and the output power are the evaluation parameters, while the independent variables were gasification temperature (923–1,223 K), equivalence ratio (0.1–0.6) and steam-to-biomass ratio (0.1–1.5).

The empirical prediction models of produced hydrogen yield and output power were statistically analyzed using an ANOVA (analysis of variance) as shown in Supplementary Table S3. The terms of “A, B, and C” refer to gasification temperature, equivalence ratio, and steam-to-biomass ratio, respectively. Generally speaking, a p-value of less than 0.05 indicates a significant term in the regression model (Cuevasglory et al., 2017). Both the gasification temperature (A) and ER (B) were highly correlated with the production yield of hydrogen and the system output power. Both models were considered significant since p-values were less than 0.001. R-squared values of 0.9988 and 0.9976 for the hydrogen production model and output power model are observed, respectively. Additionally, “Adeq Precision” measures the signal-to-noise ratio, and a value greater than 4 is desirable. The values of the models (45.28, 39.30) indicate adequate signals. Therefore, both models are desirable to navigate the design space.

From Figure 6, it can be seen that the yield of hydrogen increased with the increasing equivalence ratio under the condition of relatively low equivalence ratio. When the equivalence ratio exceeded a certain level, the hydrogen yield turned down. An appropriate ER value could maximize the hydrogen production yield. Temperature and steam-to-biomass ratio made same impacts. From the empirical regression model, the highest hydrogen production was calculated as 41.28 (mol/kg) at conditions of 1,031.73 K, 0.325, and 0.886 (temperature, equivalence ratio, and steam-to-biomass ratio).

Figure 7 shows the effects of gasification temperature, ER, and S/B on output power. The energy recovery system which utilizes the heat of the exhaust gas transfers energy to the ORC system, and the heat of gasifier outlet syngas increases with the gasification temperature and S/B. Therefore, larger operating parameters (gasification temperature and S/B) can improve the output power of the ORC system. The highest output power was calculated as 4,733.11 (kW) at conditions of 1,223 K, 0.579, and 1.5 (temperature, equivalence ratio, and steam-to-biomass ratio). Figures 6D and 7D show the actual and predicted response values of the regression model. The values were concentrated near the line, which indicated that it is a reliable regression model with small errors.
The equation in terms of actual equation can be used as the regression model to make predictions, while the coded coefficients are useful for identifying the relative impact of the factors by comparing the factor coefficients. Actual factors should not be used to determine the relative impact of each factor because the coefficients are scaled to accommodate the units of each factor, and the intercept is not at the center of the design space. As shown in Supplementary Table S4, the coded coefficients for the hydrogen production yield were gasification temperature \( (A = -1.46) \), equivalence ratio \( (B = -5.06) \), and steam-to-biomass ratio \( (C = -0.73) \), which indicated that the equivalence ratio was the major influential independent variable. The influential coded coefficients contributing to the increasing output power were the linear terms of gasification temperature \( (A = 866.00) \), equivalence ratio \( (B = 790.34) \), and steam-to-biomass ratio \( (C = 633.79) \). Gasification temperature was the major parameter contributing to the increasing output power since the heat exchanger could recover more energy into the ORC system with the increasing gasification temperature.

**Multi-Objective Optimization Results**

The formulated multi-objective optimization (MOO) problem for the designed system is shown in Table 7. In this study, two important optimization objectives were studied using the genetic algorithm method (NSGA-II) incorporated in Python: 1) maximization of hydrogen production yield and 2) maximization of output power (Li et al., 2019).

### Table 7 | MOO problem formation and the objective function values at points A, B, and C.

| Ranges | A       | B       | C       |
|--------|---------|---------|---------|
| Decision variables |         |         |         |
| Gasification temperature (K) | 923–1,223 | 1,223 | 1,123.74 | 1,031.73 |
| Equivalence ratio | 0.10–0.60 | 0.58 | 0.328 | 0.325 |
| Steam-to-biomass ratio | 0.10–1.50 | 1.50 | 1.50 | 0.89 |
| Object variables |         |         |         |
| H\textsubscript{2} yield (mol/kg) | – | 11.44 | 39.31 | 41.28 |
| Output power (kW) | – | 4,733.11 | 3,558.08 | 2,572.91 |

**FIGURE 7** | Response surface and the effect of operating conditions on power generation from wood chips: (A) S/B: 1.05, (B) ER: 0.35, (C) temperature: 1,023 K, and (D) actual vs. predicted plot.
The objectives functions for each point on the Pareto front, as well as the optimal solution (Zhiyuan et al., 2017). The LINMAP method (linear programming technique for multidimensional analysis of preference) was used to find the preferred optimal solution (Zhiyuan et al., 2017). The LINMAP method is executed with the following three steps:

- The points of the Pareto front curve are made nondimensional by Eq. 24.
- The distances (norms) of the points on the Pareto front from the ideal point which has the best value for both objective functions are obtained with Eq. 25.
- The point with the lowest distance is selected as the preferred optimal solution (point B).

\[
f_{1}^{*} = \sqrt{\frac{f_{1}}{\sum(f_{1})}}, \quad f_{2}^{*} = \sqrt{\frac{f_{2}}{\sum(f_{2})}}
\]

\[
d_{i} = \sqrt{w_{1}(f_{1}^{*} - f_{1}^{*\text{ideal}})^{2} + w_{2}(f_{2}^{*} - f_{2}^{*\text{ideal}})^{2}}
\]

In the above equations, \(f_{1}^{*}\) and \(f_{2}^{*}\) are the nondimensional objective function values for each point on the Pareto front, while \(f_{1}^{*\text{ideal}}\) and \(f_{2}^{*\text{ideal}}\) represent the nondimensional objective function values for the ideal point. \(w_{1}\) (hydrogen yield) and \(w_{2}\) (output power) are the weighting factors to balance the relative importance of both objectives. In this study, \(w_{1}\) and \(w_{2}\) were set to be equally important (i.e., \(w_{1} = w_{2} = 1\)), and point B is the preferred optimal solution. Eventually, the value of objectives and major decision variables at points A, B, and C are listed in Table 7.

**Figure 8** depicts the Pareto frontier diagram of the optimal solution points of the proposed model (Pareto frontier).

**CONCLUSION**

An equilibrium model based on the Gibbs free energy minimization method was modified by correcting the carbon conversion efficiency and the nonequilibrium factors. The model was validated by comparing with the experimental data from wood chips and sorghum in fluidized bed reactors. The hydrogen yield of wood chips was highest among the four kinds of biomass under the same working condition because of its high volatile and hydrogen content. The Box–Behnken method for a statistical analysis was applied to study the effect of gasification temperature, equivalence ratio, and steam-to-biomass ratio on the hydrogen production yield and output power. The equivalence ratio was the most significant factor affecting the hydrogen production yield, while gasification temperature had the greatest influence on the system power output. The highest hydrogen production was predicted to be 41.28 (mol/kg) at conditions of 1,031.73 K, 0.325, 0.886 (gasi temperature, equivalence ratio, and steam-to-biomass ratio), while the maximum output power was produced as 4,733.11 (kW) at conditions of 1,223 K, 0.579, 1.5 (gasification temperature, equivalence ratio, and steam-to-biomass ratio) from the established regression models. A preferred optimal solution with the hydrogen yield of 39.31 (mol/kg) and output power of 3,558.08 (kW) was achieved when considering the hydrogen yield and power output as the equally important objectives.

**DATA AVAILABILITY STATEMENT**

All datasets presented in this study are included in the article/Supplementary Material.

**AUTHOR CONTRIBUTIONS**

XZ: method, investigation, and writing. YZ and XJ: resources. YF: review and editing. QD: conceptualization, writing, and supervision.

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**Supplementary Material**

All datasets presented in this study are included in the article/Supplementary Material.
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SUPPLEMENTARY MATERIAL

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