Dynamic Modeling Data Return by Using BEKK-GARCH (Study: PT. Indofarma Tbk (INAF) and PT. Kimia Farma Tbk (KAEF) from June 2015 to July 2020)

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Abstract. The Vector Autoregressive (VAR) model is a statistical model that can be used for modeling multivariate time series data which is commonly applied in the fields of finance, management, business and economics. However, economic data, especially return values, have quite high data fluctuations, so we need to add the Generalized Autoregressive Conditional Heteroscedasticity (GARCH) model in the analysis to obtain efficient results. This study will discuss the formation of the best model for multivariate time series data, namely return data of PT. Indofarma Tbk. (INAF) and PT. Kimia Farma Tbk. (KAEF) from June 2015 to July 2020, where data returned for the two variables tended to have a high volatility shock at some time and low volatility at other times which characterizes the data as having an ARCH effect so that the GARCH model will be used in this analysis, namely the BEKK-model. GARCH. This model proposes a new parameterization which is easily given a restriction, namely the requirement that \( H_t \) must be positive for all values of \( \varepsilon_t \) and \( x_t \) in sample room. Based on the selection of the best model using the AICC, HQC, AIC and SBC criteria, it is found that the VAR (1)-GARCH (1,1) model is the best model for the data used. Then this research will also examine the behavior and relationship between INAF and KAEF based on Granger Causality and Impulse Response. In addition, based on the forecasting results of the VAR (1)-GARCH (1,1) model, it shows that this model is good for short-term forecasting.

Keywords: Forecasting, Vector Autoregressive (VAR), GARCH, BEKK-GARCH

1. Introduction
Time series data is data that is observed based on time in a certain period. According to Brockwell and Davis, the time series model with observational data \( \{x_t\} \) is a specification of the shared distribution of a sequence of random variables \( \{X_t\} \) where \( \{x_t\} \) is postulated as the realization [1]. In time series analysis, there are several models such as autoregressive (AR), moving average (MA) models or a combination of the two models, namely the Autoregressive moving average (ARMA). The three models are time series analysis which involves modeling the mean. This analysis is commonly used in
economics, finance, and capital markets [2]. In the capital market game, investors are investing with the aim of getting profits in the future [3]. As for this benefit, investors must analyze the stock price by looking at the return of the stock price to make buy and sell decisions in investing [4]. Stock return itself is the level of profit enjoyed by investors for an investment they do [5]. Investors will get profits or capital gains when the return value is positive, whereas if the return value is negative, the investor will get a loss or capital loss. Therefore, making decisions must be good in order to avoid losses, so we need to do an appropriate analysis, namely time series analysis. However, usually an investor does not only invest in one company but several companies so that there is not only one stock return data that needs to be analyzed so that investors know the stock return movements of all the companies that they invest in. So, in this case the univariate time series analysis can no longer be relied upon, but instead will use multivariate time series analysis. Multivariate time series analysis was developed by Tiao and Box by analyzing time series from several time series data simultaneously [6]. This analysis is widely discussed in several literatures and is often used in forecasting in various fields such as finance, economics, geography, and capital markets [7; 8]. The model that is commonly used and effective in forecasting multivariate time series data is Vector Autoregressive (VAR). VAR was developed by Sims [9] as an alternative to the simultaneous equation approach [10; 1]. The application of the use of the Vector Autoregressive (VAR) model itself has been widely used, such as by Stock and Watson, Sharma et. al., Warsono et. al., and Kesumah et. al. who performed dynamic modeling of stock prices data [11; 12; 13; 14].

Return is one of the factors that motivates investors to invest and tends to have variants that change over time [15]. The fluctuation and risk of stock returns are illustrated by the volatility of the data. Volatility is a statistical measurement for the fluctuation in the price of an investment during a certain period which plays an important role in the fields of investment, securities valuation and risk management [16]. Volatility has been widely used in various studies, especially in the fields of economics and finance, including research by Mascaro and Meltzer; Belongia; Engle and Susmel; Karolyi; and Engel and Gifyaczi [17; 18; 19; 20; 21]. Lopez and Walter evaluated the VaR covariance matrix using constant, historical, EWMA, GARCH and implied volatility models [22]. If there is a wide range of price fluctuations in a short period of time, this indicates high volatility and low volatility if prices move slowly [23]. The difference in volatility fluctuation indicates that the variance of the residual is variable or not constant, so it is called heteroscedasticity [24; 25].

Heteroscedasticity data requires an additional method, namely Autoregressive Conditional Heteroscedasticity (ARCH) to overcome heterogeneous variants. Meanwhile, for multivariate time series data that has heteroscedasticity, the Multivariate Autoregressive Conditional Heteroscedasticity (Multivariate-ARCH) was introduced by Engle, Granger and Kraft to make it more efficient [26]. This model was later extended or generalized by Bollerslev, Engle and Woolridge to become Multivariate-GARCH which involves variance modeling or error modeling [27]. The Multivariate-GARCH model is practical and relatively easy to use in estimating volatility and is considered the basis for dynamic volatility models [28]. Research that uses the Multivariate GARCH includes Francq and Zakoian in their research on asset prices and risk management which crucially depends on the conditional covariance structure of portfolio assets [29]. As well as Bumi, which examines and compares the return volume of Indonesian stocks with Malaysia and Singapore [30]. A further development was built on the CCC-GARCH model by Bollerslev [31]. The BEKK GARCH model introduced by Baba, et. al. was further developed by Engle and Kroner [32; 33]. In analyzing the effects of the volatility of stock returns, the BEKK GARCH method tends to be more profitable than the GARCH model in general [34]. Engle and Kroner proposed a parametric model with positive precision constraints thus providing an effective model for modeling volatility [33]. BEKK GARCH is known for its ease of obtaining a positive definite variance-covariance matrix and its efficiency in reducing the number of parameters estimated. According to Rahman and Serletis, BEKK GARCH is used to estimate covariance conditions, and can also be used to estimate conditional correlations indirectly [35]. Some researchers who have conducted research related to the BEKK GARCH model are Caporin and McAleer, Xinjun and Minhui, and Hongfei and Lou [36; 37; 38].
So that in this study we will be modeling the best model selection from stock price return data from Indonesian pharmaceutical companies, namely PT. Indofarma Tbk. (INAF) and PT. Kimia Farma Tbk. (KAEF) from June 2015 to July 2020. This study will apply modeling involving mean and error modeling, namely the VAR-BEKK GARCH model so that a model is formed that can describe the dynamic model of the two variables. In addition, this study will also examine the behavior and relationship of the two variables based on the Granger Causality test and Impulse analysis of each variable.

2. Statistical Model

Time series analysis is an analysis for data in a past time period which is useful for obtaining forecasts of future conditions. However, if there are several observations from several variables that will be analyzed simultaneously, the analysis used is the Multivariate Time Series analysis. The model that is often used in Multivariate Time Series analysis is the Vector Autoregressive Moving Average (VARMA). The VARMA model explains the relationship between observations and errors of a variable at a certain time with observations and errors in the variable itself and other variables at the previous time. Here are some classifications of the VARMA model, namely:

2.1. Vector Autoregressive Model (VAR)

The VAR model is often used to determine the habits of the variables simultaneously over time [12]. VAR model was introduced by Sims as a tool to analyze macroeconomic data. VAR model treats all involved variables symmetrically [9]. In the VAR model, a vector consists of two or more variables and on the right side contains the lag vector of the dependent. The VAR (p) model can be written as follows:

\[ Y_t = \sum_{i=1}^{p} \varphi_i Y_{t-1} + a_t \]

where \( Y_t \) is nx1 vector at time \( t \), \( \varphi_i \) is nxn matrix, \( i = 1, 2, \ldots, p \), where \( p \) is lag length, and \( a_t \) is vector shock. By using backshift operator, we have

\[ (1 - \varphi_1 B - \varphi_2 B^2 - \ldots - \varphi_p B^p)Y_t = a_t \]

where \( B^jY_t = Y_{t-j} \) where \( j = 1, 2, \ldots, p \). and \( \varphi_p = [\varphi_{lm}^s] \) is kxk matrix and \( s = 1, 2, \ldots, p \).

2.2. Generalized Autoregressive Conditional Heteroscedastic (GARCH)

Generalized Autoregressive Conditional Heteroscedasticity (GARCH) model is a development of Autoregressive Conditional Heteroscedasticity (ARCH). This model was developed to avoid the high order of the ARCH model, and to choose a simpler model, thus ensuring that the variance is always positive. The GARCH model can be written as follows:

\[ X_t = \delta + \sum_{i=1}^{p} \varphi_i X_t + \varepsilon_t - \sum_{i=1}^{q} \theta_i \varepsilon_{t-i} \]

\[ \varepsilon_t = N(0, \sigma_t^2) \]

\[ \sigma_t^2 = \lambda_0 + \sum_{i=1}^{q} \lambda_i \varepsilon_{t-i}^2 + \sum_{j=1}^{p} \beta_j \sigma_{t-j}^2 \]

Where \( X_t \) is conditional mean [39].

Model GARCH multivariate is defined as follows:

\[ r_t = \mu_t + \alpha_t \]

\[ \alpha_t = H_t^{-1/2} z_t \]

where, \( r_t \) : nx1 vector data at time \( t \).

\( a_t \) : nx1 vector of mean-corrected data at time \( t \).

\( \mu_t \) : nx1 vector of expected value of the conditional \( r_t \).

\( H_t \) : nxn matrix of conditional variance \( a_t \) at time \( t \).

\( Z_t \) : nx1 vector of \( \varepsilon \sim iid \)
2.3. BEKK GARCH

This model was first proposed by Baba, Engle, Kraft, and Kroner and then further developed by Engle and Kroner [32; 33]. Although two of the original originators no longer joined, the new parameterization is still given the acronym BEKK. Engle and Kroner proposed a new parameterization that is easily restrictive of the requirement that $H_t$ be positive for all values of $\epsilon_t$ and $x_t$ in the sample space [33].

This model can be written in the following equation:

$$
H_t = C_0^* C_0^* + \sum_{k=1}^{K} C_{1k}^* x_t C_{1k}^* + \sum_{k=1}^{K} \sum_{l=1}^{q} A_{1k}^* \epsilon_{t-l} \epsilon_{t-l} A_{1k}^* + \sum_{k=1}^{K} \sum_{l=1}^{q} G_{1k}^* H_{t-l} G_{1k}^* 
$$

where $C_0^*$, $A_{1k}^*$ and $G_{1k}^*$ are nxn matrix parameters where $C_0^*$ triangular, $C_{1k}^*$ is Jxn matrix parameters, and summation by the limit K determines the general state of the process. This explains that the above equation will be positive for sure in weak conditions.

When the model GARCH(1,1) with $K=1$ and if there is no exogenous effect, model (3) becomes:

$$
H_t = C_0^* C_0^* + A_{11}^* \epsilon_{t-1} \epsilon_{t-1} A_{11}^* + G_{11}^* H_{t-1} G_{11}^* 
$$

Model (4) can be translated into vector and diagonal representations as follows:

$$
H_t = \begin{bmatrix} h_{11,t} & h_{12,t} & h_{22,t} \\ 0 & 0 & 0 \\ \end{bmatrix} 
$$

$$
= \begin{bmatrix} C_0^* C_0^* & 0 & 0 \\ 0 & 0 & 0 \\ \end{bmatrix} 
$$

$$
+ \begin{bmatrix} a_{11} & a_{12} & a_{21} & a_{22} \\ a_{21} & a_{22} & 0 & 0 \\ \end{bmatrix} \begin{bmatrix} \epsilon_{1(t-1)} & \epsilon_{2(t-1)} \\ \epsilon_{2(t-1)} & 0 \\ \end{bmatrix} \begin{bmatrix} a_{11} & a_{12} & a_{21} & a_{22} \\ a_{21} & a_{22} & 0 & 0 \\ \end{bmatrix} 
$$

$$
+ \begin{bmatrix} g_{11} & g_{12} & g_{21} & g_{22} \\ g_{12} & g_{22} & 0 & 0 \\ \end{bmatrix} \begin{bmatrix} h_{11(t-1)} & h_{12(t-1)} & h_{21(t-1)} & h_{22(t-1)} \\ h_{12(t-1)} & h_{22(t-1)} & 0 & 0 \\ \end{bmatrix} \begin{bmatrix} g_{11} & g_{12} & g_{21} & g_{22} \\ g_{12} & g_{22} & 0 & 0 \\ \end{bmatrix} 
$$

$$
(5)
$$

3. Data Analysis

In this study, the data used are daily stock return data from the pharmaceutical sector, namely Indofarma Tbk. (INAF) and Kimia Farma Tbk. (KAEF) from June 2015 to July 2020 obtained from idnfinancial.com and the Indonesia Stock Exchange (IDX) with a plot series distribution form of the two variables can be selected in Figure 1. The use of return data was chosen because it more describes the risk of changes in stock prices itself. It can be seen that INAF return data has a higher data fluctuation than KAEF. In addition, INAF and KAEF experienced changes in data fluctuations which were quite unstable from January to June 2020. This was based on the COVID-19 pandemic so that pharmaceutical sector stocks attracted the attention of investors. Therefore, time series analysis will be carried out to determine the future stock return forecast in order to determine the risk of the INAF and KAEF stocks. However, in conducting time series analysis, there are assumptions that must be met first, namely stationarity. The method of testing the standard used is the Dickey-Fuller Test, the results of which can be seen in Table 1.
In the Augmented Dicky-Fuller test, the H0 test is rejected if Pr < Tau is less than 0.05, and based on Table 1. The Pr < Tau value of each type for all variables, both INAF and KAEF, is <0.0001 which means <0.05. Therefore the decision obtained is to reject H0 or in other words, stationary data [40; 1]. This decision is also in line with the trend graphs from INAF and KAEF which are presented in Figure 2. The trend graph shows that the ACF and PACF values of ADRO and ITMG did not decrease exponentially, which means that the data used in the study were stationary, so that further analysis can be carried out.

**Table 1. Dickey-Fuller Unit Root Test**

| Variable | Type     | Rho   | Pr < Rho | Tau    | Pr < Tau |
|----------|----------|-------|----------|--------|----------|
| INAF     | Zero Mean| -1576.2| 0.0001   | -28.06 | <.0001   |
|          | Single Mean| -1582.4| 0.0001   | -28.11 | <.0001   |
|          | Trend     | -1582.6| 0.0001   | -28.10 | <.0001   |
| KAEF     | Zero Mean| -1682.7| 0.0001   | -28.99 | <.0001   |
|          | Single Mean| -1686.3| 0.0001   | -29.01 | <.0001   |
|          | Trend     | -1689.3| 0.0001   | -29.03 | <.0001   |

**Figure 1.** Plot Data Return share price INAF and KAEF from June 2015 - July 2020

**Figure 2.** Plot Trend and Correlation Analysis for (a) INAF and (b) KAEF
Whereas in Figure 3 we can see the form of the volatility of the INAF and KAEF conditional variances. Figure 4 (a) shows that INAF has several high volatility shocks and has low volatility at other times which characterizes that INAF is heteroscedasticity. While the KEAF volatility presented in Figure 4 (b) shows that the volatility is more stable than INAF, but there are still 3 shocks that exceed 0.01 and in the 1700 to 1800 period there is a volatility shock that is not high enough, while in other time periods KAEF is relatively volatile low. So, based on the volatility condition of the KAEF data, it can be seen that the KAEF return data is heteroscedastic. In addition, to further ascertain whether the two data have heteroscedasticity or not, further testing will be carried out, namely the White Noise Test as presented in Table 2.

In this White Noise test, the null hypothesis is that the residual does not have an ARCH effect (data is not heteroscedasticity) and the alternative hypothesis is that the data has an ARCH effect (heteroscedasticity data) with a significance level of $\alpha = 0.05$, $H_0$ will be rejected if the $p$-value <0.05. Based on Table 2. It is obtained that the $Pr> F$ value of the INAF and KAEF variables is <0.0001 which means <0.05 so we reject $H_0$ which in other words that the data we have contains heteroscedasticity. Therefore, we will include the GARCH model in the VARMA modeling that will be formed, namely the BEKK-GARCH model to overcome the heteroscedasticity characteristic. Furthermore, model testing will be carried out based on the AICC, HQC, AIC and SBC criteria from the VAR (1) -GARCH (1,1), VAR (2) -GARCH (1,1), VAR (3) -GARCH (1) models, 1), VAR (4) -GARCH (1,1), and VAR (5) -GARCH (1,1) to get the best model from the data. Based on the model criteria information presented in Table 3. Where the criteria for selecting the model criteria for AICC, HQC, AIC and SBC show that VAR (1) -GARCH (1,1) has the smallest criterion value compared to other models and the VAR (1) -GARCH model (1,1) has the schematic representation of parameters and GARCH parameters which are presented in Table 4. And Table 5. Thus, the best model for the INAF and KAEF return resized data is the VAR (1) -GARCH (1,1) model.

![Figure 3. Plot Conditional Variance INAF (a) and KAEF (b)](image)

| Variable | Durbin Watson | Normality | ARCH |
|----------|---------------|-----------|------|
|          |               | Chi-Square | Pr > ChiSq | F Value | Pr > F |
| INAF     | 1.78116       | 7573.30   | <.0001    | 153.30  | <.0001 |
| KAEF     | 1.89662       | 9999.99   | <.0001    | 92.75   | <.0001 |
A conditional mean GARCH (1,1) model is obtained as follows:

\[
\begin{align*}
\text{VAR(1)-} & \quad \text{GARCH(1,1)} \quad \text{VAR(2)-} \quad \text{GARCH(1,1)} \quad \text{VAR(3)-} \quad \text{GARCH(1,1)} \quad \text{VAR(4)-} \quad \text{GARCH(1,1)} \quad \text{VAR(5)-} \quad \text{GARCH(1,1)} \\
\text{AICC} & \quad -21423.7 \quad -21402.4 \quad -21384.8 \quad -21367.8 \quad -21354.5 \\
\text{HQC} & \quad -21393.4 \quad -21364.1 \quad -21338.5 \quad -21313.6 \quad -21292.3 \\
\text{AIC} & \quad -21424.0 \quad -21402.8 \quad -21385.4 \quad -21368.6 \quad -21355.6 \\
\text{SBC} & \quad -21340.9 \quad -21297.7 \quad -21258.1 \quad -21219.2 \quad -21184.0
\end{align*}
\]

Table 3. Information Criteria of Models

| Model     | Variable/Lag | AR1           |
|-----------|--------------|---------------|
| VAR (1) - | INAF         | ..            |
| GARCH (1,1)| KAEF         | .+            |

+ is > 2*std error, - is < -2*std error, . is between, * is N/A

Table 4. Schematic Representation of Parameter Estimates

| Model     | Variable/Lag | GCHC | ACH1 | GCH1 |
|-----------|--------------|------|------|------|
| VAR (1) - | h1           | ++   | .    | .    |
| GARCH (1,1)| h2           | +    | .    | .    |

+ is > 2*std error, - is < -2*std error, . is between, * is N/A

Based on the selection of the best model, the VAR (1) -GARCH (1,1) model is obtained as the best model. Therefore, it will be carried out estimating the model parameters presented in Table 6 and the GARCH model parameters presented in the Table. But in Table 7, it is known that there are 2 insignificant parameters ACH1_2_1 and ACH1_1_2, but based on the principle of meaning where the parameter value is greater than 0.05. ACH1_2_1 is still included in the model so that the VAR (1) -GARCH (1,1) model is obtained as follows:

\[
[ \text{ADRO}_t \text{ ITMG}_t ] = [0.01412 0.03704 - 0.03137 0.07178 ][\text{INAF}_{t-1} \text{ KAEF}_{t-1} ] + [\varepsilon_{1t} \varepsilon_{2t} ]
\]

Conditional mean of model VAR (1) can be written as univariate models as follows:

\[
\begin{align*}
\text{INAF}_t & = 0.01412 \text{ INAF}_{t-1} + 0.03704 \text{ KAEF}_{t-1} + \varepsilon_{1t} \quad (6) \\
\text{KAEF}_t & = -0.03137 \text{ INAF}_{t-1} + 0.07178 \text{ KAEF}_{t-1} + \varepsilon_{2t} \quad (7)
\end{align*}
\]

and conditional variance of model GARCH (1,1) with the BEKK GARCH method is:

\[
\begin{align*}
\text{h}_{11t} & = 0.00036 + (0.58787)^2 \varepsilon_{1(t-1)}^2 + (0.76182)^2 \text{h}_{11(t-1)} + \\
& \quad 2(0.58787)(0.05905) \varepsilon_{1(t-1)} \varepsilon_{2(t-1)} + (0.05905)^2 \varepsilon_{2(t-1)}^2 + \\
& \quad 2(0.76182)(-0.08835) \text{h}_{12(t-1)} + (-0.08835)^2 \text{h}_{22(t-1)} \\
\text{h}_{12t} & = 0.00018 + (0.58787)(0.03779)\varepsilon_{1(t-1)}^2 + (0.52986)(0.05905)\varepsilon_{2(t-1)}^2 + \\
& \quad (0.76182)(-0.03379)\text{h}_{11(t-1)} + \\
& \quad (0.75486)(-0.08835)\text{h}_{22(t-1)} + (0.76182)^2 \text{h}_{11(t-1)} + \\
& \quad (0.05905)(0.00018) + (0.58787)(0.52986)\varepsilon_{1(t-1)}\varepsilon_{2(t-1)} +
\end{align*}
\]
\[(0.01295)(-0.07361) + (0.92956)(1.01948)h_{12(t-1)}\]

\[
h_{22t} = 0.00027 + (0.52986)^2 \varepsilon_{2(t-1)}^2 + (0.75486)^2 h_{22(t-1)} + 2(0.52986)(0.03779) \varepsilon_{2(t-1)} \varepsilon_{2(t-1)} + (0.03779)^2 \varepsilon_{2(t-1)}^2 + 2(-0.03379)(0.75486) h_{12(t-1)} + (-0.03379)^2 h_{11(t-1)}\]

The statistical tests of the ADRO_t and ITMG_t models are presented in Table 6. Based on these statistical tests, the INAF_t model has a value of F = 15.91 and a P-Value <0.0001 which means significant and has a coefficient of determination of R-square 0.0084. While KAEF_t has a value of F = 14.30 and P-Value = 0.0002 which means significant and has a coefficient of determination of R-square 0.0076. So it can be said that the two univariate models are feasible to use. Model (6) explains that the return value of KAEF has a positive effect on lag 1 (t-1). Model (7) explains that the INAF return value has a negative effect on lag 1 (t-1). In addition, based on Figure 6, it can be seen that the INAF return distribution tends to approach the normal distribution. Meanwhile, if seen from the patterns of prediction error, it can be seen that KAEF has a more stable prediction error than INAF. However, the prediction error from INAF and KAEF shows high instability compared to other years, namely in 2020.

| Equation | Parameter | Estimate | Standard Error | t Value | Pr > | Variable |
|----------|-----------|----------|----------------|---------|-------|----------|
| INAF     | AR1_1_1   | 0.01412  | 0.02997        | 2.17    | 0.0376| INAF(t-1)|
|          | AR1_1_2   | 0.03704  | 0.02599        | 2.45    | 0.0143| INAF(t-1)|
| KAEF     | AR1_2_1   | -0.03137 | 0.01580        | -1.99   | 0.0473| KAEF(t-1) |
|          | AR1_2_2   | 0.07178  | 0.02865        | 2.51    | 0.0123| KAEF(t-1) |

| Parameter | Estimate | Standard Error | t Value | Pr > | |
|-----------|----------|----------------|---------|-------|-------|
| GCHC1_1   | 0.00036  | 0.00004        | 9.18    | 0.0001|
| GCHC1_2   | 0.00018  | 0.00003        | 6.57    | 0.0001|
| GCHC2_2   | 0.00027  | 0.00003        | 8.52    | 0.0001|
| ACH1_1_1  | 0.58787  | 0.04565        | 12.88   | 0.0001|
| ACH1_2_1  | 0.05905  | 0.06679        | 0.88    | 0.3767|
| ACH1_1_2  | 0.03779  | 0.02270        | 1.67    | 0.0961|
| ACH1_2_2  | 0.52986  | 0.04101        | 12.92   | 0.0001|
| GCH1_1_1  | 0.76182  | 0.02503        | 30.43   | 0.0001|
| GCH1_2_1  | -0.08835 | 0.04475        | -1.97   | 0.0485|
| GCH1_1_2  | -0.03379 | 0.01707        | -1.98   | 0.0479|
| GCH1_2_2  | 0.75486  | 0.03136        | 24.07   | 0.0001|
Table 8. Univariate Model Anova Diagnostics

| Variable | R-Square | Standard Deviation | F Value | Pr > F |
|----------|----------|--------------------|---------|--------|
| INAF     | 0.0084   | 0.04816            | 15.91   | <.0001 |
| KAEF     | 0.0076   | 0.03687            | 14.30   | 0.0002 |

Furthermore, a Granger Causality Test will be carried out which aims to determine the causal relationship between variables [41; 13]. The Granger Causality test is based on the Wald test where the Chi-square distribution or F-test is used as an alternative. Based on the results of the Granger Causality test analysis presented in Table 9, it shows that the first test in which INAF is group 1 and KAEF is Group 2, the Chi-square value = 11.23 and P-value = 0.0008, which means the data reject H0. Therefore, it is concluded that the INAF return value is influenced by the KAEF return value. Meanwhile, for the second test with KAEF as group 1 and INAF as group 2, it was obtained Chi-square = 0.57 and P-value = 0.4491, so we don't have enough evidence to reject H0. In other words, it can be concluded that the KAEF return value is not affected by the INAF return value. In addition to the Granger Causality test, the relationship of variables from the multivariate time series analysis is also explained through the IRF interpretation presented in Figures 5 and 6.
Table 9. Granger Causality Wald Test

| Test | Group          | DF | Chi-Square | Pr > ChiSq |
|------|----------------|----|------------|------------|
| 1    | Group 1 Variabels: INAF | 1  | 11.23      | 0.0008     |
|      | Group 2 Variabels: KAEF  |    |            |            |
| 2    | Group 1 Variabels: KAEF  | 1  | 0.57       | 0.4491     |
|      | Group 2 Variabels: INAF  |    |            |            |

Figure 5. Response to Impulse in INAF

Figure 6. Response to Impulse in KAEF

Impulse response itself is commonly used in economics to describe the economic reaction from time to time to exogenous impulse. The horizontal axes in Figures 5 and 6 show the time periods where
one period represents one day. While the vertical axis shows changes in a variable to the shock itself and other variables. Figure 5 (a) shows the impulse of INAF on itself. The shock of the INAF standard deviation causes a fluctuating response until the 3rd period then the response goes to zero or stability. Whereas in Figure 5 (b) it can be seen that the fluctuation of the standard deviation tends to increase after receiving a KAEP shock and reaching the equilibrium point in the 3rd period. Meanwhile, Figure 6 (a) depicts the impulse of KAEP's response to INAF shock. The shock from the standard deviation KAEP tends to decrease after receiving a shock from INAF and in the 3rd period it starts to move towards stability. Meanwhile, in Figure 6 (b) the shock from the standard deviation of ITMG caused ITMG to stabilize or move towards zero in the 3rd period.

| Variable | OBS | Time   | Forecast | Standard Error | 95% Confidence Limits |
|----------|-----|--------|----------|----------------|-----------------------|
| INAF     | 1876| 20JUL2020 | -0.00033 | 0.02844 | -0.05607 | 0.05542 |
|          | 1877| 21JUL2020 | -0.00003 | 0.03314 | -0.06498 | 0.06492 |
|          | 1878| 22JUL2020 | -0.00000 | 0.03686 | -0.07225 | 0.07225 |
|          | 1879| 23JUL2020 | -0.00000 | 0.03994 | -0.07828 | 0.07828 |
|          | 1880| 24JUL2020 | -0.00000 | 0.04254 | -0.08338 | 0.08338 |
|          | 1881| 25JUL2020 | -0.00000 | 0.04478 | -0.08776 | 0.08776 |
|          | 1882| 26JUL2020 | -0.00000 | 0.04672 | -0.09157 | 0.09157 |
|          | 1883| 27JUL2020 | 0.00000  | 0.04843 | -0.09491 | 0.09491 |
|          | 1884| 28JUL2020 | 0.00000  | 0.04993 | -0.09787 | 0.09787 |
|          | 1885| 29JUL2020 | 0.00000  | 0.05128 | -0.10050 | 0.10050 |
|          | 1886| 30JUL2020 | 0.00000  | 0.05247 | -0.10285 | 0.10285 |
|          | 1887| 31JUL2020 | 0.00000  | 0.05355 | -0.10496 | 0.10496 |
| KAEP     | 1876| 20JUL2020 | -0.00063 | 0.02523 | -0.05007 | 0.04881 |
|          | 1877| 21JUL2020 | -0.00004 | 0.02851 | -0.05592 | 0.05585 |
|          | 1878| 22JUL2020 | -0.00000 | 0.03100 | -0.06075 | 0.06075 |
|          | 1879| 23JUL2020 | -0.00000 | 0.03296 | -0.06460 | 0.06460 |
|          | 1880| 24JUL2020 | -0.00000 | 0.03453 | -0.06768 | 0.06768 |
|          | 1881| 25JUL2020 | -0.00000 | 0.03582 | -0.07020 | 0.07020 |
|          | 1882| 26JUL2020 | 0.00000  | 0.03687 | -0.07226 | 0.07226 |
|          | 1883| 27JUL2020 | 0.00000  | 0.03774 | -0.07397 | 0.07397 |
|          | 1884| 28JUL2020 | 0.00000  | 0.03847 | -0.07540 | 0.07540 |
|          | 1885| 29JUL2020 | 0.00000  | 0.03908 | -0.07659 | 0.07659 |
|          | 1886| 30JUL2020 | 0.00000  | 0.03959 | -0.07759 | 0.07759 |
As it is known that the purpose of time series analysis is to obtain forecasts of future conditions based on previous observational data. Therefore, forecasting of INAF and KAEF return data will be formed in the next 12 days based on model VAR (1) -GARCH (1,1) which is presented in Table 10. Based on the forecast results it can be seen that the return value of both INAF and KAEF in the first 2 days of forecasting gives a negative value, which means that the share value has decreased or lost to investors, while from the 3rd to 12th day forecasting it gives a value of 0 (zero) which means that there is no significant change in the stock price of both INAF and KAEF. In addition, based on Figure 7, it can be seen that ADRO and ITMG have predicted values and the observational data are close to each other, this indicates that the model is fit with the data. Meanwhile, in the plot forecasts for INAF and forecasts for KAEF, it can be seen that the confidence interval tends to increase, this shows that the model used is suitable and good for analyzing and forecasting short-term data.

4. Conclusion
Based on the analysis that has been done, the best model in forecasting and modeling PT Indofarma Tbk daily stock return data, (INAF) and PT. Kimia Farma Tbk. (KAEF) from June 2015 to July 2020 is a VAR (1) -GARCH (1,1) model. The selection of the best model uses several model selection criteria,
namely AICC, HQC, AIC and SBC where all the criteria produce the smallest VAR (1) -GARCH (1,1) value. In addition, based on the granger causality test, it is known that the INAF stock return variable is not only influenced by itself but is also influenced by the KAEF variable, while the KAEF variable is only influenced by itself. Then based on the forecasting results obtained based on the model that has been formed, it is found that the prediction values are close to each other with the observational data which means the model is fit with the data. It can also be seen that the confident interval of forecasting INAF and KAEF data for the next 12 days tends to increase. Thus, it can be concluded that VAR (1) - GARCH (1,1) is suitable for modeling INAF and KAEF return data for the short term.

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