TRANSIT CONFIRMATION AND IMPROVED STELLAR AND PLANET PARAMETERS FOR THE SUPER-EARTH HD 97658 b AND ITS HOST STAR

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Received 2014 January 2; accepted 2014 February 25; published 2014 April 8

ABSTRACT

Super-Earths transiting nearby bright stars are key objects that simultaneously allow for accurate measurements of both their mass and radius, providing essential constraints on their internal composition. We present here the confirmation, based on Spitzer transit observations, that the super-Earth HD 97658 b transits its host star. HD 97658 is a low-mass ($M_*=0.77\pm0.05M_\odot$) K1 dwarf, as determined from the Hipparcos parallax and stellar evolution modeling. To constrain the planet parameters, we carry out Bayesian global analyses of Keck–High Resolution Echelle Spectrometer (Keck-HIRES) radial velocities and Microvariability and Oscillations of Stars (MOST) and Spitzer photometry. HD 97658 b is a massive ($M_p=7.55^{+0.83}_{-0.79}M_\oplus$) and large ($R_p=2.247^{+0.092}_{-0.091}R_\oplus$ at 4.5 μm) super-Earth. We investigate the possible internal compositions for HD 97658 b. Our results indicate a large rocky component, of at least 60% by mass, and very little H–He components, at most 2% by mass. We also discuss how future asteroseismic observations can improve the knowledge of the HD 97658 system, in particular by constraining its age. Orbiting a bright host star, HD 97658 b will be a key target for upcoming space missions such as the Transiting Exoplanet Survey Satellite (TESS), the Characterizing Exoplanet Satellite (CHEOPS), the Planetary Transits and Oscillations of stars (PLATO), and the James Webb Space Telescope to characterize thoroughly its structure and atmosphere.

Key words: binaries: eclipsing – planetary systems – stars: individual (HD 97658) – techniques: photometric – techniques: radial velocities

Online-only material: color figures, machine-readable table

1. INTRODUCTION

Among the diversity of the exoplanetary population, the class of the so-called “super-Earths,” with a mass of a few Earth masses, is of utmost interest. First, they do not exist in the solar system, leaving us with only extrasolar planets for detailed studies. Second, they seem to be extremely common in the Galaxy (Fressin et al. 2013; Petigura et al. 2013; Howard 2013).

Third, a wide variety of interiors are theoretically possible for a small range of radii ($1-R_p/R_\oplus<5$) and masses ($1-M_p/M_\oplus<10$), from pure iron composition with no atmosphere to water planets with a significant atmosphere (Valencia et al. 2007; Seager et al. 2007). Transiting super-Earths around bright nearby stars are therefore key objects that allow for accurate measurements of both their mass and radius (Gillon et al. 2012a). Equally important, they also allow for atmospheric measurements from transit transmission spectroscopy (e.g., Berta et al. 2012) or occultation (secondary eclipse) emission spectroscopy (Demory et al. 2012) without the challenging task of resolving the planet’s light from that of its host star. Such direct imaging is only possible to date for widely separated, massive young planets (Marois et al. 2010; Absil et al. 2013; Kuzuhara et al. 2013). Transiting super-Earths around bright nearby stars are therefore essential for shedding light on their true nature and origin.

HD 97658 is the second-brightest ($V=7.7$, $K=5.7$) host star found to be transited by a super-Earth (the brightest being 55 Cnc; Winn et al. 2011; Demory et al. 2011). HD 97658 b was detected from radial velocity (RV) measurements with Keck–High Resolution Echelle Spectrometer (Keck-HIRES) spectroscopy, with a minimum mass $M_p = 8.2 \pm 1.2 M_\oplus$ and an orbital period $P = 9.494 \pm 0.005$ days (Howard et al. 2011). The detection of transits from ground-based observations was announced (Henry et al. 2011), but follow-up space-based Microvariability and Oscillations of Stars (MOST) photometry showed no transits at the claimed ephemeris (Dragomir et al. 2012). Further MOST observations finally discovered transit events with an ephemeris consistent with that predicted from RV measurements (Dragomir et al. 2013). From a global Markov Chain Monte Carlo (MCMC) analysis simultaneously modeling HIRES RVs and MOST photometry, they derived a $2.34^{+0.15}_{-0.15} R_\oplus$ and 7.86 ± 0.73 $M_\oplus$ planet, confirming its super-Earth nature with an average density of $3.44^{+0.91}_{-0.82}$ g cm$^{-3}$.

The announcement of transit detections by Dragomir et al. (2013) motivated us to include HD 97658 b in our Spitzer program to search for and observe transits of low-mass RV-detected
planets (Gillon et al. 2011). HD 97658 b was observed in 2013 August with the Spitzer Infrared Array Camera (IRAC; Fazio et al. 2004) at 4.5 μm. Spitzer already proved to be the tool of choice to perform unequivocally precise and continuous photometry for the detection and characterization of the ultrashallow transits of super-Earths such as HD 40307 b (for which transits are firmly discarded; Gillon et al. 2010) and 55 Cnc e (Demory et al. 2011). We present here the confirmation of the transiting nature of HD 97658 b from Spitzer observations. We also present global Bayesian analyses of Keck–HIRES RV data and MOST and Spitzer photometry in order to derive as accurately as possible the parameters of HD 97658 b.

Ultimately, the precision for planetary parameters is related to the precision achieved for the stellar parameters because planetary masses and radii as determined by transit and RV measurements cannot be determined independently from the properties of their host stars. Atmospheric stellar parameters such as effective temperature $T_{\text{eff}}$ and metallicity are determined from spectroscopy. The stellar radius, at least for nearby stars, can be derived from the luminosity (from parallax measurements) and the spectroscopic effective temperature using the classical equation of stellar physics $L_*=4\pi R_*^2 T_{\text{eff}}^4$. Obtaining the stellar mass is a more delicate process that can be achieved by a stellar evolution code using $T_{\text{eff}}$, metallicity, and luminosity as inputs. The stellar age is usually poorly constrained in this process (Soderblom 2010). A powerful method for providing accurate and precise stellar radius, mass, and age is asteroseismology, by modeling the oscillation spectrum of the star. The Convection, Rotation, and planetary Transits (CoRoT; Baglin et al. 2006) and Kepler (Koch et al. 2010) space missions were based on this complementarity, whereas the future Transiting Exoplanet Survey Satellite (TESS; Ricker et al. 2010) and Planetary Transits and Oscillations of stars (PLATO; Rauer et al. 2014) space missions will also include significant asteroseismic programs. We also investigate here how future asteroseismic observations of HD 97658 can help to further improve the knowledge of the star and planet parameters.

This paper is organized as follows. The Spitzer observations and their reduction are presented in Section 2, while host star modeling is presented in Section 3. Section 4 is devoted to the analysis of the Spitzer data, while Section 5 presents global Bayesian analyses of RV, MOST, and Spitzer data. We discuss the results and provide avenues to further improve the characterization of HD 97658 b and its host star in Section 6. Conclusions and prospects are given in Section 7.

2. SPITZER PHOTOMETRY

We monitored HD 97658 with Spitzer’s IRAC camera on 2013 August 10 from 13:01:00 to 18:27:00 UT, corresponding to a transit window\textsuperscript{11} as computed from the August 10 from 13:01:00 to 18:27:00 UT, corresponding to a

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\textsuperscript{11} The “transit window” is the window of time within which the transit is likely to occur.

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\textsuperscript{12} http://sha.ipac.caltech.edu/applications/Spitzer/SHA

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of its planets because they are expected to have formed within a few million years of each other. Two sources are available for the atmospheric stellar parameters of HD 97658 (Howard et al. 2011; Henry et al. 2011). From Howard et al. (2011, respectively, Henry et al. 2011), the effective temperature is \( T_{\text{eff}} = 5170 \pm 44 \) K (respectively, \( T_{\text{eff}} = 5119 \pm 44 \) K), the surface gravity \( \log g = 4.63 \pm 0.06 \) (respectively, 4.52 \( \pm \) 0.06), and \([\text{Fe/H}] = -0.23 \pm 0.03 \) (respectively, \(-0.30 \pm 0.03\)). We assumed here that \([\text{Fe/H}]\) represents the global metallicity with respect to the Sun, defined as \([\log(Z/X)_\odot - \log(Z/X)]\), where \(X\) and \(Z\) are the fractional mass of hydrogen and elements heavier than helium, respectively. A Hipparcos parallax measurement of HD 97658 is available: \( \pi = 47.36 \pm 0.75 \) mas (van Leeuwen 2007), giving a distance of 21.11 \( \pm \) 0.34 pc. Using observed magnitudes of Koen et al. (2010) and bolometric corrections of Flower (1996) (with \( M_{\text{bol}} = 4.73;\) Torres 2010), this translates to a stellar luminosity of \( L_*/L_\odot = 0.355 \pm 0.018\). As is standard, all of the errors cited in this section and throughout the paper are in the 1\( \sigma \) range (68.3% probability).

We used the effective temperature, metallicity, and luminosity with their respective errors as inputs for stellar evolution modeling with the Code Liégeois d’Évolution Stellaire (CLES) code (Scuflaire et al. 2008b). In all evolutionary computations we used the mixing-length theory (MLT) of convection (Böhm-Vitense 1958) and the Coulomb Eggleton Faulkner Flanery (CEFF) equation of state (Christensen-Dalsgaard & Dauppen 1992). We considered here the most recent solar mixture\(^{14}\) of Asplund et al. (2009), giving for the present Sun \( (Z/X)_\odot = 0.0181\). We used for this metallic mixture the Opacity at Livermore (OPAL) opacity tables (Iglesias & Rogers 1996) for the high temperatures and the ones of Ferguson et al. (2005) for the low temperatures. The surface boundary conditions are given by atmospheres computed within the Eddington approximation. Microscopic diffusion (gravitational settling) is taken into account, but no radiative accelerations of metals were included given the low mass we expect for the host star (Escobar et al. 2012). For the same reason, no convective core is expected, so no overshooting was considered here. Finally, the \( \alpha \) parameter of the MLT was kept fixed to the solar calibration (\( \alpha_{\text{MLT}} = 1.8 \)). Because the helium atmospheric abundance cannot be directly measured from spectroscopy in low-mass stars such as HD 97658, we computed evolutionary tracks with three initial helium abundances: the solar value, a value labeled \( Y_G \) that increases with \( Z \) (as expected if the local medium follows the general trend observed for the chemical evolution of galaxies; Izotov & Thuan 2010), and an arbitrary value \( Y_{\text{arb}} = 0.26 \) close to the most recent primordial value from the big bang nucleosynthesis (Izotov & Thuan 2010).

\(^{14}\) “Mixture” is stellar physics jargon that means the proportions of \( X, Y, \) and \( Z \), with \( X + Y + Z = 1 \).

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### Table 1

| BJD\(_{\text{UTC}}\) (day) | Flux | Error | \( dX \) (pixel) | \( dY \) (pixel) | FWHM | FWHM\(_X\) | FWHM\(_Y\) | sky | e" |
|--------------------------|------|-------|-----------------|-----------------|-------|------------|------------|-----|-----|
| 6523.0421407213          | 1.00042472 | 6.56049341e-04 | 15.99832813 | 16.06571875 | 1.1364 | 1.28568133 | 1.32744292 | 4.489830 |
| 6523.0422367211          | 1.00001116 | 6.42787543e-04 | 16.0106250 | 16.06018178 | 1.1312 | 1.27501281 | 1.31006923 | 3.548975 |
| 6523.0423342212          | 0.99991553 | 5.79276271e-04 | 16.0089063 | 16.05589373 | 1.1294 | 1.27034785 | 1.2574292 | 4.898830 |
| 6523.0424312213          | 1.00127259 | 6.76242624e-04 | 16.0063937 | 16.0600000 | 1.1361 | 1.28203944 | 1.32744292 | 3.624313 |
| 6523.0425283214          | 0.99966335 | 6.49723786e-04 | 15.98585937 | 16.07169037 | 1.1443 | 1.30291407 | 1.33813047 | 3.095959 |

(This table is available in its entirety in a machine-readable form in the online journal. A portion is shown here for guidance regarding its form and content.)

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![Figure 2](https://example.com/figure2.png)

**Figure 2.** Evolutionary tracks in a log \( T_{\text{eff}} - \log(L_*/L_\odot) \) diagram for HD 97658, for various masses and metallicities that respect the observational constraints \( (L_*/L_\odot, [\text{Fe/H}]) \). Several initial mixtures, in particular for the helium abundance \( (Y_G, Y_{\text{arb}}, Y_{\text{arb}}) \) were also considered (see text for details). The age of the star when it crosses the 1\( \sigma \) box \( \log(T_{\text{eff}} - \log(L_*/L_\odot)) \) is also indicated.

(A color version of this figure is available in the online journal.)

We computed many evolutionary tracks for several masses with the constraints of having consistent metallicities and effective temperatures as given by spectroscopy and having luminosities consistent with the one derived from the Hipparcos parallax. No stellar models younger than the universe were found to have a luminosity \( L_*/L_\odot = 0.355 \pm 0.018 \) within the 1\( \sigma \) range of effective temperature and metallicity given by Henry et al. (2011), which are therefore discarded from stellar evolution modeling. Within the 1\( \sigma \) range given by Howard et al. (2011) for the metallicity and effective temperature, the values of stellar mass are \( M_* = 0.77 \pm 0.05 M_\odot \) (Figure 2). Unfortunately, no useful constraints on the stellar age were obtained: such stars can reach \( L_*/L_\odot = 0.355 \pm 0.018 \) when they are a few Gyr old only if they are \( \sim 0.82 M_\odot \), but they can be much older, up to the age of the universe, if they are less massive (see Figure 2). This also strongly depends on the initial mixture. All evolutionary tracks that respect the observational constraints on \( T_{\text{eff}}, L_* \), and \([\text{Fe/H}]\) correspond to stars that are on the main sequence in the H-core burning phase.

Combining the stellar luminosity \( L_*/L_\odot = 0.355 \pm 0.018 \) with the effective temperature of Howard et al. (2011) results in a stellar radius \( R_*/R_\odot = 0.74 \pm 0.03 \). These values are
somewhat different from the ones cited by Howard et al. (2011) and also by Henry et al. 2011 (which were taken by Dragomir et al. 2013). The discrepancy comes from their announced luminosity $L_*/L_\odot = 0.30 \pm 0.02$ and absolute magnitude $M_V = 6.27 \pm 0.10$, which are not consistent with the *Hipparcos* parallax (van Leeuwen 2007; see also Table 1 of Koen et al. 2010, HD 97658 $\equiv$ HIP 54906).

4. SPITZER CONFIRMS THE TRANSITING NATURE OF HD 97658 b

The *Spitzer* light curve was analyzed with the adaptive MCMC algorithm presented in Gillon et al. (2012b, and references therein), with the aim to confirm or refute the transiting nature of HD 97658 b and the ephemeris of Dragomir et al. (2013). The MCMC algorithm is a Bayesian inference method based on stochastic simulations that sample the posterior probability distributions of adjusted parameters for a given model. Our MCMC implementation uses the Metropolis–Hasting algorithm (see, e.g., Carlin & Louis 2008) to perform this sampling. Our nominal model was based on a star and a transiting planet on a Keplerian orbit about their center of mass. We modeled the eclipse photometry with the photometric eclipse model of Mandel & Agol (2002), multiplied by a baseline model representing the low-frequency instrumental effects. This baseline model was a sum of a second-order polynomial in the $x$ and $y$ positions of the PSF center, first-order polynomials in the width of the PSF in the $x$ and $y$ directions, and a first-order polynomial of the logarithm of time. The two first kinds of polynomial aimed to model the “pixel-phase effect” affecting the IRAC InSb arrays, whereas the last one represented the sharp increase of the *Spitzer* detectors’ response, generally called “the ramp” in the literature (see, e.g., Knutson et al. 2008). This baseline model was elected based on the minimization of the Bayesian information criterion (Schwarz 1978). The final global photometric model (eclipse model multiplied by the baseline model) is shown by the red curve in Figure 1, which nicely illustrates the importance of detrending operations on *Spitzer* raw photometry in order to extract the scientific information. Finally, quadratic limb-darkening was assumed, with values deduced from the tables of Claret & Bloemen (2011) for the appropriate *Spitzer* filters and stellar parameters.

The jump parameters, i.e., the parameters over which the MCMC random walk (here made of 10 chains of $10^4$ steps) occurred, were the transit depth $dF$, the transit width ($W$), the transit timing (time of minimum light) $T_0$, and the impact parameter $b' = a \cos i/R_*$, $i$ the orbital inclination and $R_*$ the radius of the planet. We assumed a uniform prior distribution for all of these jump parameters. The orbital period $P$ was also a jump parameter but this time with a Gaussian prior based on the value from Dragomir et al. (2013). In our MCMC implementation, it means that we imposed a Bayesian penalty:

$$BP_{\text{ephemeris}} = \frac{(P - P_{\text{D13}})^2}{\sigma_{P_{\text{D13}}}^2},$$

(1)

where $P_{\text{D13}} = 9.4909$ days and $\sigma_{P_{\text{D13}}} = 0.0016$ days (Dragomir et al. 2013). Gaussian priors were also imposed on the stellar mass, luminosity, effective temperature, and metallicity (see Section 3), i.e., we also applied a Bayesian penalty similar to Equation (1) for these parameters. The merit function used in our MCMC simulation was therefore the sum of the $\chi^2$ for each data set (quadratic sum of the difference between the model and the data) and of the Bayesian penalties. It is also important to include stellar parameters with their Gaussian priors in the MCMC simulation to properly propagate the errors and to accurately derive the physical parameters from the jump parameters. If a jump parameter is not constrained by observational data, its a posteriori distribution will be the same as its a priori distribution, but we can use the resulting distribution to propagate errors correctly.

The good convergence and the quality of the sampling of the MCMC simulation were successfully checked using the statistical test of Gelman & Rubin (1992), by verifying that the so-called potential reduction factors for all jump parameters are close to unity (within 1%). Figure 3 shows the *Spitzer* IRAC photometry corrected for the systematics and binned into 5 minute wide intervals with the best-fitting eclipse model superimposed. The vertical lines show the propagated (17 planetary orbits later) MOST midtransit time, with 1σ errors, of Dragomir et al. (2013). The *Spitzer*-detected transit at $T_0 = 2456523.12544^{+0.00062}_{-0.00059}$ (BJD$_{\text{TDB}}$) thus fully confirms, within 1σ, the ephemeris provided by Dragomir et al. (2013).

5. GLOBAL BAYESIAN ANALYSES

In order to get the strongest constraints on the system parameters, we performed several global Bayesian analyses using as input data not only our *Spitzer* transit photometry but also the detrended MOST transit light curves (Dragomir et al. 2013) and the 171 published Keck–HIRES RVs acquired and reduced using the same techniques as in Howard et al. (2011) and compiled by Dragomir et al. (2012, 2013).

5.1. Keck–HIRES RV and Spitzer Photometry Data

We performed an MCMC simulation made of 10 chains of $5 \times 10^4$ steps including HIRES RV data and *Spitzer* photometry. We used a classical Keplerian model for the RVs (no Rossiter–McLaughlin effect was detected). The jump parameters in our MCMC simulation were the transit depth $dF$, the
transit width (from first to last contact) \( W \), the transit timing (time of minimum light) \( T_0 \), the impact parameter \( b' = a \cos i / R_s \), the orbital period \( P \), the two parameters \( \sqrt{e} \cos \omega \) and \( \sqrt{e} \sin \omega \) (\( e \) is the eccentricity and \( \omega \) the argument of periastron), and the \( K_2 \) parameter (related to the RV orbital semiamplitude \( K \) via \( K_2 = K \sqrt{1 − e^2} P^{1/3} \)). We also allowed the quadratic limb-darkening coefficients \( u_1 \) and \( u_2 \) to float in this MCMC simulation, using as jump parameters not these coefficients themselves but the combinations \( c_1 = 2u_1 + u_2 \) and \( c_2 = u_1 − 2u_2 \) to minimize the correlation of the obtained uncertainties (Holman et al. 2006). The prior distributions of these limb-darkening coefficients directly depend on the ones on the effective temperature and metallicity, for which Gaussian priors, i.e., Bayesian penalties similar to Equation (1), were imposed (\( T_{\text{eff}} = 5170 \pm 50 \) K and \( \text{[Fe/H]} = −0.23 \pm 0.03 \)). Gaussian priors were also imposed on the stellar mass (\( M_\ast = 0.77 ± 0.05 \, M_\odot \)) and luminosity (\( L_\ast = 0.355 ± 0.018 \, L_\odot \)). Again, it is important to include these parameters with their Gaussian priors in the MCMC simulation in order to correctly propagate the errors and to accurately derive the physical parameters from the jump parameters.

Table 2 shows the median values and 68.3% probability interval for the jump parameters mentioned above given by our MCMC simulation of Spitzer photometry and Keck–HIRES RVs as well as the derived stellar and planetary physical parameters. The good convergence and the quality of the sampling of the 10 chains of the MCMC simulation were successfully checked using again the Gelman & Rubin (1992) statistical test (all jump parameters have potential reduction factors near unity within 1%).

5.2. Keck–HIRES RV, MOST, and Spitzer Data

Finally, we repeated the global Bayesian analysis, but this time including the three continuous MOST transits. We only used these three light curves acquired when the star was fully in the continuous viewing zone of the satellite, the two other light curves showing a much poorer quality due to gaps in coverage and higher levels of correlated noise. As discussed in Dragomir et al. (2013), the MOST reduction pipeline suppresses the depth of a transit signal, by an amount of \( \sim 10\% \), as indicated by transit injection tests in these three MOST transits. To include this effect...
This may be related to some instrumental systematics in the photometry: we note that our planet radius based on HD 97658 b, as we discuss in the next section. The dilution effect. This could also be related to the atmospheric jump parameters, the same Gaussian priors, and the same check for the convergence and sampling quality as in Section 5.1. The temperature parameters, the same Gaussian priors, and the same check for the convergence and sampling quality as in Section 5.1. The radial velocity systematics. “CF” stands for core fraction, and “hh” is for bulk hydrogen and helium by mass: (1) core fraction = 0, H–He = 0, and water/ices = 0.5; (2) core fraction = 0, H–He = 0, and water/ices = 0.5; (3) core fraction = 0, H–He = 0, and water/ices = 0.5; (4) core fraction = 0, H–He = 0, and water/ices = 0.5.

(A color version of this figure is available in the online journal.)

and the uncertainty on it, we assumed a dilution of 10% ± 2% for the MOST photometry. We carried out a global MCMC analysis with the same number of steps and chains, the same jump parameters, the same Gaussian priors, and the same check of the convergence and sampling quality as in Section 5.1. The most interesting result is the transit depth in visible, from MOST photometry: $dF_{\text{MOST}} = 949_{-75}^{+81} \text{ppm}$. This translates to a planet radius $R_P = 2.49_{-0.13}^{+0.14} R_\oplus$, larger at the $2\sigma$ level than the planet radius at 4.5 $\mu$m derived from Spitzer photometry (Table 2). This may be related to some instrumental MOST systematics not fully corrected beyond the 2% uncertainty we took here on the dilution effect. This could also be related to the atmospheric composition of HD 97658 b, as we discuss in the next section. We note that our planet radius based on MOST photometry is slightly higher than the one found by Dragomir et al. (2013) ($2.34_{-0.18}^{+0.18} R_\oplus$), although it is within their 1$\sigma$ uncertainties. This is directly related to the more luminous and, therefore, larger radius star we modeled (see Section 3).

6. DISCUSSION

6.1. HD 97658 b, A Key Object for Super-Earth Characterization

6.1.1. Internal Composition of HD 97658 b

Our MCMC results (see Table 2) give a planetary radius of $R_P = 2.247_{-0.095}^{+0.098} R_\oplus$ as measured in the IRAC 4.5 $\mu$m channel and a planetary mass of $M_P = 7.55_{-0.83}^{+0.83} M_\oplus$. This yields a super-Earth with an intermediate average density ($\rho_P = 3.90_{-0.70}^{+0.70} \text{g cm}^{-3}$), close to the average density of Mars ($\rho_M = 3.9335 \text{g cm}^{-3}$). Valencia et al. (2006) proposed a model for the mass–radius relationship for rocky planets as $M_P = a R_P^3$, where $a$ depends on the composition. For the same composition, the average density of a planet therefore increases as $\rho_P \sim M_P / R_P^3$. Given that HD 97658 b is 75 times more massive than Mars, it clearly has a much lighter composition.

In Figure 4 we show how HD 97658 b compares to the other detected low-mass planets for which we have measured mass and radius. It is worth noting that the mass and radius of HD 97658 b are very similar to Kepler 68 b (Gilliland et al. 2013). To illustrate that HD 97658 b has both a low H–He content and a high core-mass fraction, within the limitations of a mass–radius diagram, we show mass–radius relations (blue lines) for four specific compositions, calculated at $T_{\text{eq}} = 700 \text{K}$: 1. a water planet (no core and no H–He) (dotted blue line); 2. core fraction of 50% and no H–He (dash-dotted line); 3. core fraction of 50% and H–He = 25% (long dashed line); 4. core fraction of 90% and H–He = 1% (solid line).

A water-only composition (1) sits above the data for HD 97658 b, even though it has no H–He. If we consider larger core-mass fractions, only those above 50% ((2)–(4)) start to approach the data for HD 97658 b. If we include any amount of H–He the amount of core needs to be larger. One possible composition for HD 97658 b is a planet with an Earth-like core of 90%, 1% H–He, and 9% water/ices (Figure 4).

It is not possible to show all the possible compositions for a low-mass planet using a mass–radius diagram; for this we resort to a ternary diagram (Figure 5). We computed various theoretical internal structures using the internal structure model described in Valencia et al. (2013), suitable for rocky and gaseous planets. Ternary diagrams relate the composition in terms of Earth-like nucleus fraction, water+ices fraction, and H–He fraction to total mass, to the radius for a specific planetary mass. Each vertex corresponds to 100%, and the opposite side to 0% of a particular component, by mass. The color bar shows the radius in terms of Earth radii, and the gray lines are the isoradius curves labeled in terms of Earth radii. The possible compositions for HD 97658 b are in the lower right corner of Figure 5.
Figure 5. Ternary diagram for HD 97658 b. This diagram shows the radius for all possible compositions for a planet of a specific mass (in this case 7.55 M⊕). Each point depicts a unique planetary composition from a combination of H–He, H₂O + ices, and rocky Earth-like nucleus (33% iron core below a 67% silicate mantle). Each vertex corresponds to 100% of each compositional end member (with H–He on top, H₂O + ices in the lower left corner, and Earth-like nucleus on the lower right corner), with 0% on the opposite line. The color bar shows the radius in terms of Earth radii, and the gray lines are the isoradius curves labeled in terms of Earth radii. The black shaded region in the lower right corner shows the possible compositions for HD 97658 b, and the width of the shaded region takes into account the uncertainty in the mass and radius (for all combinations between M ± ΔM, R ± ΔR, and M ± ΔM, R ± ΔR, with ΔM and ΔR the 1σ error in mass and radius). This compact planet has at least 60% Earth-like nucleus by mass and between 0%–40% bulk water+ices content.

(A color version of this figure is available in the online journal.)

Figure 5 (shaded in black) and correspond to a bulk composition of H–He of less than 2%, water+ices 0%–40%, and rocks in excess of 60%. The maximum H–He is obtained for a rock fraction of 92%–95% and the rest water+ices. If the planet had no water, the amount of H–He would be less than 8 × 10⁻³ by mass. If it had no H–He, the amount of water+ices is 15%–40% by mass (the range reflects the 1σ errors in mass and radius). In comparison, GJ 1214 b admits at most 7% of H–He, and it could be made out of 100% water+ices (although very unlikely). Furthermore, GJ 1214 b permits a very large range in rocky component (0%–97%), whereas HD 97658 b is more compact and requires a large proportion of rocks (60%–99%), thus requiring a formation mechanism that captures enough solid material. Unfortunately, as discussed in Valencia et al. (2013), internal structure models do not constrain the mixing ratio between H–He and water+ices in the atmosphere. Thus, they are limited in guiding spectroscopic studies, which we discuss in the next section.

6.1.2. Constraints on Atmospheric Composition

Transmission spectra of super-Earths can provide constraints on the atmospheric composition of the day–night terminator region of the planetary atmosphere, in particular on the mean molecular weight (MMW) of the atmosphere (e.g., Miller-Ricci et al. 2009) or on the presence of thick clouds. The atmospheric compositions of super-Earths are a subject of active debate at present because it is unknown if their atmospheres are H/He-rich like those of ice giants in the solar system or if they are rich in heavier molecules such as H₂O, CO, or N₂, like those of terrestrial planets. Detailed transmission spectroscopy has been reported for only one super-Earth to date, GJ 1214 b, for which the observations indicate a flat spectrum over a wide wavelength range of ~0.5–5 μm (e.g., Bean et al. 2010; Berta et al. 2011; Désert et al. 2011; de Mooij et al. 2012). The featureless spectrum of GJ 1214 b suggests the likely presence of thick clouds in the atmosphere (Howe & Burrows 2012; Miller-Ricci Kempton et al. 2012; Benneke & Seager 2013; Morley et al. 2013; Kreidberg et al. 2014), which might be obscuring the spectral features of volatile species under the cloud cover, due to which its atmospheric composition is still unknown.

In this section, despite the only 2σ significance of the planetary radius discrepancy between MOST and Spitzer data, and the possibility of instrumental MOST systematics not fully corrected (see Section 5.2), we attempted to interpret the origin of the discrepancy based on atmospheric modeling of HD 97658 b. We also assumed here that the stellar variability of HD 97658 is weak enough to infer atmospheric constraints directly from the transit-depth measurements. With a projected rotational velocity of 0.5 ± 0.5 km s⁻¹, a magnetic cycle at least 6 yr long, and a stellar rotation of 38.5 ± 1 days (Henry et al. 2011), HD 97658 is most probably a very quiet star. Furthermore, occulted star-spots leave a clear structure in the transit light curve, which we do not observe with MOST or with Spitzer.

The transit-depth measurements in the two bandpasses, the MOST bandpass in the visible centered at 0.525 μm and the Spitzer IRAC bandpass in the infrared at 4.5 μm, place complementary constraints on the atmospheric composition.
data are inconsistent (at the 2σ level) with models binned in the bandpasses. As discussed in the text, the H2O-rich scenario is also not favored by the data because such a model predicts significantly lower transit depth in the visible MOST bandpass than observed, by 2σ. We found that a cloud-free H2-rich atmosphere with subsolar C and O abundances, by a factor of 20 below solar or lower, is able to match both of the data points at the ∼1σ uncertainties. The low C and O abundances in such a model lower the H2O, CO, and CO2 absorption in order to match the low 4.5 μm transit depth, whereas the ambient H2-rich composition contributes Rayleigh scattering in the visible wavelengths, which together with Na and K absorption matches the high transit depth in the MOST bandpass. Whereas this model fits the data reasonably well, the peculiar composition with low C and O abundances poses interesting theoretical questions for future investigation.

The observations, if interpreted in the context of atmospheric modeling, are more readily explained by an atmosphere with significant Mie scattering due to hazes. We considered atmospheres with a wide range of haze compositions and particle sizes based on the models of Howe & Burrows (2012). We found that the observations can be explained by the presence of tholin hazes in a solar-abundance H2-rich atmosphere, as shown in Figure 7. The models include monodispersed tholin hazes placed uniformly in the upper atmosphere, in the 10−3–10−6 bar pressure range, in an otherwise solar-abundance atmosphere. The models shown in Figure 7 range in particle sizes between 0.01 and 0.1 μm and particle densities of 102–106 cm−3. All of the models show a steep rise in the transmission spectrum in the visible wavelengths due to Mie scattering due to the hazes, thereby explaining the high observed transit depth in the 0.525 μm MOST bandpass. Of the models shown in Figure 7, the best-fitting model contains 0.1 μm particles with a number density of 100 cm−3, but it is only a marginally better fit relative to the two other models.

To conclude this discussion, we stress that future observations at higher resolution and higher precision are definitely needed to confirm the atmospheric modeling interpretation as presented here and to further constrain the atmospheric composition of HD 97658 b.
Table 3

| Model | \(M_\odot\) | Age (Gyr) | \(T_{\text{eff}}\) (K) | \(L_\odot\) | [Fe/H] | \(\Delta \nu\) (\(\mu\)Hz) | \(\delta \nu_{\text{O2}}\) (\(\mu\)Hz) |
|-------|---------|----------|----------------|--------|--------|----------------|----------------|
| 1     | 0.73    | 11.0     | 5144           | 0.337  | −0.26  | 188.5          | 9.5            |
| 2     | 0.73    | 11.9     | 5165           | 0.348  | −0.26  | 185.8          | 8.8            |
| 3     | 0.73    | 12.8     | 5187           | 0.362  | −0.26  | 182.9          | 8.1            |
| 4     | 0.73    | 13.7     | 5210           | 0.377  | −0.26  | 179.7          | 7.3            |
| 5     | 0.77    | 7.2      | 5130           | 0.338  | −0.23  | 191.4          | 11.8           |
| 6     | 0.77    | 8.0      | 5144           | 0.346  | −0.23  | 189.0          | 11.2           |
| 7     | 0.77    | 9.0      | 5170           | 0.361  | −0.23  | 185.8          | 10.3           |
| 8     | 0.77    | 10.0     | 5195           | 0.377  | −0.23  | 182.4          | 9.5            |
| 9     | 0.81    | 1.1      | 5152           | 0.337  | −0.20  | 199.6          | 15.4           |
| 10    | 0.81    | 2.0      | 5171           | 0.346  | −0.20  | 196.6          | 14.7           |
| 11    | 0.81    | 2.9      | 5192           | 0.358  | −0.20  | 193.8          | 14.0           |
| 12    | 0.81    | 4.1      | 5220           | 0.375  | −0.20  | 190.4          | 13.2           |

6.2. Improving the Knowledge of the Host Star

An accurate knowledge of the host star is essential to deriving accurate planet parameters, as illustrated here by the importance of modeling properly the stellar luminosity and radius. Age is also a very important datum because it is expected to be equal to the age of the planet. For low-mass stars such as HD 97658, the stellar age is essentially unconstrained by the comparison with evolutionary tracks. Based on \(\log P_\text{rot}\) and \(P_\text{rot}\) calibrations, the stellar age is around 6.0 ± 1.0 Gyr (Henry et al. 2011). However, the physics behind these two empirical methods is not fully understood, and their calibrations may also present large unknown systematics that are not reflected in the 1.0 Gyr error announced (Soderblom 2010). The \(UVW\) space velocities, as measured from Hipparcos (van Leeuwen 2007), are small. This indicates that HD 97658 has thin disk kinematics, from which no useful constraints on its age can be obtained. Asteroseismology, the study of the oscillations of stars, can improve this situation (for the general principles of asteroseismology and some of the most recent achievements, see Aerts et al. 2010). In solar-type (roughly mid-F to mid-K types) stars, oscillations correspond to acoustic waves (also called \(p\)-modes) that depend on the radially varying density and internal speed of sound in the star. The power pulsation spectra of solar-type stars exhibit characteristic structures with regular spacings between the peaks. Among them, two are of utmost importance: the mean large separation \(\Delta \nu\) (\(\equiv \langle \nu_{n+1,l} - \nu_{n,l} \rangle\)), where \(\nu\) is the frequency, \(n\) the radial order, and \(l\) the angular degree of the oscillation mode) and the small separations \(\delta \nu\) (\(\equiv \nu_{n,l} - \nu_{n-1,l+2}\)). These quantities are the first quantities that can be measured in an observed pulsation spectrum, even if the quality of the data is insufficient to extract individual \(p\)-mode frequencies (Roxburgh & Vorontsov 2006; Roxburgh 2009; Mosser & Appourchaux 2009). It can be shown that the large separation is approximately the inverse acoustic diameter of the star, which means, from homology arguments, that it scales approximately as the square root of the mean density of the star: \(\Delta \nu \propto \sqrt{\rho}\). For their part, the small separations \(\delta \nu\) provide a measure of conditions in the core of the star and hence the stellar age.

To illustrate the potential of asteroseismology to improve the knowledge of the host star, in particular by constraining its age, we computed the seismic properties of 12 selected stellar models with the Liege adiabatic oscillation code OSC (Scuflaire et al. 2008a). These models have various masses, metallicities, and ages, and all simultaneously respect the observational triplet (\(T_{\text{eff}}, L_\odot, [\text{Fe/H}]\)) within the associated \(1\sigma\) uncertainties. Their properties are presented in Table 3. We plotted in Figure 8 the \(\Delta \nu - \delta \nu_{\text{O2}}\) diagram, called the \(C - D\) diagram in the asteroseismic jargon (Christensen-Dalsgaard 1984), for these 12 stellar models. Figure 8 shows that an accuracy of \(\sim \pm 1\mu\text{Hz}\) on the large and small separations measurements will help to get improved knowledge of the stellar mass and age. The main unknown for asteroseismic observations concerns the amplitudes of the oscillations, which are not predictable by the current linear theory of stellar oscillations. The amplitudes are expected to be weak in K-type stars (Kjeldsen & Bedding 1995), but HD 97658 is a quite bright star. We estimated, from the measured CoRoT performances on similar type and magnitude stars (see the example of the K0 dwarf \(V = 7.84\) HD 46375; Gaulme et al. 2010) that a spaceborne 0.3 m mission like Characterizing Exoplanet Satellite (CHEOPS; Broeg et al. 2013) would be able to obtain such a precision from \(\sim 2-3\) months of nearly continuous observations. This may be a suggestion for the complementary CHEOPS open program. The PLATO mission, if HD 97658 falls in the observed fields, will definitely be able to measure the large and small separations with the required accuracy. The PLATO should even be able to accurately measure the individual oscillation frequencies, from which a full asteroseismic analysis can be carried out, obtaining not only very accurate global parameters (stellar mass, radius, age) but also constraints on the internal physics of the star. This is in turn important to calibrate and improve the evolutionary tracks computed from stellar evolution codes.

\[\Delta \nu = \nu_{n+1,0} - \nu_{n,0} \quad \text{and} \quad \delta \nu_{\text{O2}} = \nu_{n,0} - \nu_{n-1,2}\]. They are given for the corresponding frequency at maximum power, around which the pulsation spectrum is expected to be observed.
7. CONCLUSION AND PROSPECTS

HD 97658 b is a key transiting super-Earth. The current data from Spitzer and MOST photometry, and also Keck–HIRES RVs, analyzed with our MCMC code, indicate a planet with an intermediate average density ($\rho_p = 3.90^{+0.08}_{-0.07}$ g cm$^{-3}$). Investigating the possible internal compositions of HD 97658 b, our results indicate a large rocky component of at least 60% by mass, an amount of 0%-40% of water+ices, and very little H–He components, at most 2% by mass. If interpreted as constraints on the atmospheric composition, the transit depths in both the Spitzer and MOST brandpasses together favor either an H$_2$–rich atmosphere with hazes or a cloud-free atmosphere with a low metallicity. Six more transit observations are planned in the course of 2014 with the Spitzer IRAC camera, this time with 3.6 μm channel (PI: D. Dragomir).

HD 97658 b will be a target of the coming space missions TESS and CHEOPS, in particular to accurately measure the planet radius at visible wavelengths. By the time TESS and CHEOPS are launched (circa 2017), the Gaia mission (launched in 2013 December) is hoped to have provided extremely accurate parallax measurements, within ~10 μas for the bright nearby stars such as HD 97658. This will improve the knowledge on the distance of the star by two orders of magnitude compared to the current Hipparcos parallax. From there, the stellar radius will be known with an accuracy of 1% (assuming a ±50 K uncertainty on $T_{\text{eff}}$). Knowing the stellar radius to 1% is also what we can expect for present and near-future long baseline interferometers (Boyajian et al. 2013). This is the ultimate precision we can achieve on the planet radius, providing that the number of observed transits is sufficient to measure the transit depth $dF \propto (R_p/R)^2$ with an accuracy much below 1%. The ESA has now officially confirmed the selection of PLATO as the next M3 mission, to be launched around 2024. If HD 97658 falls in the observed fields, PLATO would not only measure the transit depth with unprecedented accuracy, but would also be able to detect oscillation frequencies of the host star that provide through asteroseismology accurate stellar mass and, very importantly, age.

Orbiting a bright K1-type star ($V = 7.7$, $K = 5.7$), HD 97658 b is a target of choice for atmospheric characterization. There is Hubble Space Telescope time allocated in the coming months to take transmission spectroscopy of HD 97658 b with the WFC3 camera in IR (PI: H. Knutson). The aim is to distinguish a large scale-height, H-dominated atmosphere from a compact, water–steam atmosphere, which will confirm or refute the constraints on the atmospheric composition derived in this work. By comparing these measurements to the few targets for which such transmission spectroscopy is currently possible (55 Cnc e and GJ 1214 b), this will provide the first measure of the diversity of super-Earth atmospheres prior to the era of the European Extremely Large Telescope and the James Webb Space Telescope.

The authors thank the referee for constructive comments that improved the quality of the manuscript. V. Van Grootel warmly thanks A. Grotsch-Noels and M.-A. Dupret for fruitful discussions on stellar modeling. The authors also thank H. Knutson for various discussions on this planet. This work is based in part on observations made with the Spitzer Space Telescope, which is operated by the Jet Propulsion Laboratory, California Institute of Technology, under a contract with NASA.

Support for this work was provided by NASA. M. Gillon is Research Associate at the Belgian Fonds de la Recherche Scientifique (FRS).

Facilities: Keck-I (HIRES), MOST, Spitzer

REFERENCES
Miller-Ricci Kempton, E., Zahnle, K., & Fortney, J. J. 2012, ApJ, 745, 3
Morley, C. V., Fortney, J. J., Kempton, E. M.-R., et al. 2013, ApJ, 775, 33
Mosser, B., & Appourchaux, T. 2009, A&A, 508, 877
Petigura, E. A., Marcy, G. W., & Howard, A. W. 2013, ApJ, 770, 69
Rauer, H., Catala, C., Aerts, C., et al. 2014, Exp. Astron., in press (arXiv:1310.0696)
Ricker, G. R., Latham, D. W., Vanderspek, R. K., et al. 2010, BAAS, 42, 215
Roxburgh, I. W. 2009, A&A, 506, 435
Roxburgh, I. W., & Vorontsov, S. V. 2006, MNRAS, 369, 1491
Schwarz, G. 1978, AnSta, 6, 461
Scuflaire, R., Montalbán, J., Théado, S., et al. 2008a, Ap&SS, 316, 149
Scuflaire, R., Théado, S., Montalbán, J., et al. 2008b, Ap&SS, 316, 83
Seager, S., Kuchner, M., Hier-Majumder, C. A., & Militzer, B. 2007, ApJ, 669, 1279
Sharp, C. M., & Burrows, A. 2007, ApJS, 168, 140
Soderblom, D. R. 2010, ARA&A, 48, 581
Stetson, P. B. 1987, PASP, 99, 191
Torres, G. 2010, AJ, 140, 1158
Valencia, D., Guillot, T., Parmentier, V., & Freedman, R. S. 2013, ApJ, 775, 10
Valencia, D., O’Connell, R. J., & Sasselov, D. 2006, Icar, 181, 545
Valencia, D., Sasselov, D. D., & O’Connell, R. J. 2007, ApJ, 665, 1413
van Leeuwen, F. 2007, A&A, 474, 653
Winn, J. N., Matthews, J. M., Dawson, R. I., et al. 2011, ApJL, 737, L18