Analysis on borehole stability of gas drilling with complete stress–strain and thermal stress theory

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Abstract

In conventional mud drilling, sufficient drilling fluid density is required to maintain wellbore stability. However, in gas drilling, the support ability of gas in wellbore is very weak, and the wellbore stability is usually good. This shows that the borehole instability mechanism of gas drilling is different from that of mud drilling. In gas drilling, the borehole wall rock still has a certain bearing capacity after reaching the peak strength. In this paper, the stability of gas drilling wellbore is studied by using the complete stress–strain model. The deformation of rock around borehole in gas drilling can be divided into elastic zone, plastic zone, and broken zone. The radii of plastic zone and broken zone were used to evaluate the stability of borehole wall. This method has a good general applicability to the case of no thermal stress in borehole wall rock. However, due to throttling and cooling as gas flows out of the bit nozzle during gas drilling, thermal stress occurs when the cryogenic flow in the annulus meets the hot formation. Therefore, thermal stress is introduced into the complete stress–strain calculation model. The radii of plastic zone and broken zone are calculated according to the actual drilling data, and compared with the measured borehole diameter. The results show that the model is reasonable and effective. Analysis shows that in gas drilling process, the borehole temperature is much lower than the original formation temperature near the bottom of the borehole, and the borehole temperature is higher than the formation temperature in the upper part of the borehole. Thermal stress has a significant effect on borehole stability. The thermal stress in the bottom borehole makes the rock shrink and offset the expansion of the original in situ stress on the surrounding rock, thus enhancing the stability of the borehole wall. The surrounding rock in the top borehole expands under the action of thermal stress, enhancing the expansion of the surrounding rock toward the borehole and aggravating the instability of the borehole wall. The model can be used to better explain the wellbore instability mechanism of gas drilling, and it is more intuitive to use plastic zone radius and broken zone to characterize wellbore stability of gas drilling.

Keywords Complete stress–strain theory · Thermal stress · Gas drilling · Strength · Elastic–plastic softening

Introduction

Gas drilling technology can improve rate of penetration, avoid lost circulation, and overcome sensitivity of formation water. The gas in the borehole is not enough weight to support the wall of borehole, and the borehole will inevitably deform because of the original in situ stress. However, in many gas drilling processes, no serious wellbore instability occurred. The theory of stability by using drilling fluid to prop up the borehole wall does not explain this phenomenon well. Generally, researchers regard rock as elastic material when analyzing the stability of borehole wall, and believe that rock failure will occur when the stress exceeds the peak strength, and use it as the limiting condition for studying the stability of borehole wall to calculate and estimate the...
collapse pressure of borehole wall. Rocks can not only bear the load before failure, but also has a certain load capacity after failure. The complete stress–strain process of rocks can more actually reflect the yield procedure and deformation characteristics of rocks.

However, the complete stress–strain model of rock is too complex to analyze the engineering problems (Yuan and Chen 1986; Chen and Yuan 1988). The estimation methods of collapse pressure is based on the hypothesis that the rock completely loses its bearing capacity after reaching the peak strength and compares the geostress around borehole with the rock strength (Wu and Lin 1987). Based on the air drilling practice in Karamay oilfield, it is put forward that the influencing factors of wellbore stability in air drilling include mechanics and chemistry (Li 1994). The concentration and chemical properties of liquid phase in mist drilling effected on borehole stability were evaluated by laboratory experiments (Huang et al. 1995). The von Mises failure criterion is used to get reliable prediction of the collapse pressure (Guo and Ghalambor 2002). A method for calculating collapse pressure of gas drilling wall is established on the base of rock elasticity theory and Mohr–Coulomb criterion (Jiang et al. 2007). The elastic–brittle-plastic constitutive model was established to analyze the stability of hard rock under high geostresses (Chen and Feng 2007). The failure modes of the deep rock mass contain brittle failure or ductile failure that depends on the property of rock mass and the geostress state (Zhou et al. 2008). The influence factor of pore pressure is studied during gas drilling in high-pressure gas zone, and the theory of rock elasticity is still used to calculate the collapse pressure (Liu et al. 2010). Triaxial compression test data of five different rocks were used to verify the unified strength criterion with four parameters (Lu and Du 2013). Rock anisotropy effected on rock strength and collapse pressure was investigated through the modified Mogi–Coulomb criterion (Yang et al. 2020). Hydraulic fracturing practices also show that the rock around borehole still maintains stability and load capacity even if it has reached the peak strength (Ding et al. 2018).

At the same time, the gas flow in the borehole temperature and pressure changes are more complex for the compressibility of gas. Ramey presented an approximate solution to the wellbore heat-transmission problem involved in injection of hot or cold fluids (Ramey 1962). The expansion factor in the yield zone and the cohesive effect of broken material is considered to develop around the excavation with an elastic zone beyond (Wilson 1980). A mathematical model was developed to evaluate wellbore heat losses and two-phase pressure drop in concentric-pipe steam injection wells (Griston and Whithee 1987). Generalized analytical models were presented to compute circulating fluid temperature in conduits for both forward- and reverse-circulation cases, as a function of circulation time and well depth (Hasan et al. 1996a, b). The difference temperature between drilling fluid and borehole wall and the thermal stress in rock around the borehole were studied (Nguyen et al. 2010; Zhang et al. 2012). Akong et al. investigated the effect of temperature on wellbore stability under thermal effects at the wellbore wall during mud drilling (Akong et al. 2011). The temperature drop of gas flow is larger than liquid flow in the borehole, especially near the bottom of hole; the temperature on the wall of borehole is lower than geothermal value (Li et al. 2015; Guo et al. 2016). Therefore, the thermal stress of the borehole should be taken into account when the stresses around the borehole are analyzed in gas drilling.

The rock around borehole will be deformed by original in situ stress because the gas pressure in the borehole during gas drilling is too low to support the borehole wall. According to the complete stress–strain model of rock, the borehole stability is analyzed. Furthermore, the phenomenon of throttling and cooling is easy to occur near the bottom of the borehole during gas drilling, and thermal stress will be generated at the borehole wall, which will also have a certain influence on the stability of the borehole wall. Therefore, a thermo-elastoplastic model is established to analyze the wellbore stability of gas drilling.

Mathematic model

Ideal elastic–plastic softening model for rocks

The curve of the complete stress–strain relation of rock (Fig. 1A) is simplified into the simplest broken line (Fig. 1B). The $a$-$c$-$f$ broken line in Fig. 1B represents an ideal elastic–plastic softening model. The simplified model divides the deformation process of rock into three stages: elastic deformation, plastic softening deformation, and residual deformation (Yuan and Chen 1986). The elastic modulus of elastic deformation is $E$, and the softening modulus of plastic softening deformation is $E_p$, so the fragility coefficient is $\beta = E_p/E$ (Guo et al. 2021; Li et al. 2017).

1. Strength of rock in the elastic deformation stage

Most rocks follow the Hooke’s law in the stage of elastic deformation and meet the Mohr–Coulomb criterion (Yang et al. 2019; AL-AJMI and ZIMME 2005, 2006) at the yield of elastic deformation; the strength function is expressed as follows:

$$
\sigma = \frac{E}{1+\beta}\epsilon
$$

where $\sigma$ is the stress, $E$ is the Young’s modulus, $\beta$ is the fragility coefficient, and $\epsilon$ is the strain. The stress–strain curve of rock is shown in Fig. 2A. When the stress is less than the yield stress, the rock is in the elastic deformation stage, and the stress–strain curve is a straight line with a slope of $E$. When the stress reaches the yield stress, the rock enters the plastic deformation stage, and the stress–strain curve becomes a concave curve. When the stress exceeds the peak stress, the rock enters the residual deformation stage, and the stress–strain curve becomes a convex curve.
where $\sigma_{\theta}$ and $\sigma_r$ are the tangential and radial stresses, MPa; $\sigma_{ce}$ is the uniaxial compressive strength in the process of elastic deformation, MPa; $\phi_e$ is the angle of internal friction of elastic deformation, degree.

2. Strength of rock in the plastic deformation stage

The rock strength attenuated with the development of deformation mainly because of the change of cohesion, and the strength of the plastic deformation is illustrated as follows:

$$\sigma_{\theta} = K_{p1}\sigma_r + \sigma_{ce}$$  \hfill (1)

$$K_{p1} = \frac{1 + \sin\phi_e}{1 - \sin\phi_e}$$  \hfill (2)

where $\sigma_{\theta}$ and $\sigma_r$ are the tangential and radial stresses, MPa; $\sigma_{ce}$ is the uniaxial compressive strength in the process of elastic deformation, MPa; $\phi_e$ is the angle of internal friction of elastic deformation, degree.

3. Strength of rock in the residual deformation stage

The strength of the rock drops to the minimum value in the residual deformation. The strength of the residual deformation is expressed as follows:

$$\sigma_{\theta} = K_{p2}\sigma_r + \sigma_{cs}$$  \hfill (3)

$$K_{p2} = \frac{1 + \sin\phi_p}{1 - \sin\phi_p}$$  \hfill (4)

where $\sigma_{\theta}$ and $\sigma_r$ are the tangential and radial stresses, MPa; $\sigma_{cs}$ is the uniaxial compressive strength of the residual deformation, MPa.

The original *in situ* stresses around borehole

It is assumed that the rock is an isotropic and homogeneous continuous medium, and the hole is in a state of plane strain under the average horizontal stress, $\sigma_o$. The equilibrium equation of stresses (Fang and Wang 1991) is

$$r \frac{\partial \sigma_r}{\partial r} + \sigma_r - \sigma_{\theta} = 0$$  \hfill (6)

With the average horizontal stress increasing, the rock around the borehole divides into three regions (Fig. 2):

![Fig. 2 Rock deformation zones around borehole](image)
elastic zone, plastic zone, and residual zone. If the average horizontal stress is weak, the elastic zone appears possibly only. Otherwise, the average horizontal stress is huge, and three zones appear inevitably.

\[
\sigma_r = \left( \frac{2\sigma_o - \sigma_{ce}}{k_{p1} + 1} + \frac{2\beta M}{k_{p2} - 1} + \frac{\sigma_{ce}}{k_{p2} - 1} \right) \left( \frac{r}{R_p} \right)^{k_{p2} - 1} - \frac{2(\sigma_{ce} + \beta M)}{k_{p2} - 1} \right) + \frac{\sigma_{cp}}{k_{p2} + 1}
\]

\[\sigma_r = k_{p2}\sigma_r + \sigma_{cp}\]  

1. Stresses in the elastic zone

According to the elasticity theory, the stresses in the elastic zone are:

\[
\sigma_r = \sigma_o - (\sigma_o - \sigma_{re})(\frac{R_p}{r})^2
\]

\[
\sigma_o = \sigma_o + (\sigma_o - \sigma_{re})(\frac{R_p}{r})^2
\]

In the elastic zone, the stresses inside the rock satisfy the Hooke’s law, and the radial stress expression at the interface of the elastic–plastic zone can be obtained by application of the Mohr–Coulomb strength criterion:

\[
\sigma_{re} = \frac{2\sigma_o - \sigma_{ce}}{k_{p1} + 1}
\]

where \(R_p\) is the radius of the plastic zone, \(m\); \(\sigma_o\) is the average horizontal geostress, MPa; \(\sigma_{re}\) is the radial stress at the interface of the elastic–plastic zone, MPa.

2. Stresses in the plastic zone

Due to the relative sliding inside the rock during the plastic deformation stage, the strength of the rock shows a decreasing trend. The strength attenuation law of the plastic zone in Eq. (3) can be expressed as follows:

\[
\sigma_{cp} = \sigma_{ce} - \beta M \left[ \left( \frac{R_p}{r} \right)^2 - 1 \right]
\]

Although the rock strength is lower than the peak strength at the stage of plastic deformation, there is still certain elastic deformation energy inside the rock, which is defined as the plastic deformation modulus. The plastic deformation modulus is defined as follows:

\[
M = \frac{(1 + \nu)(k_{p1} - 1)\sigma_o + \sigma_{ce}}{k_{p1} + 1}
\]

where \(M\) is the plastic deformation modulus, MPa; \(\beta\) is the fragility coefficient; \(\nu\) is Rock Poisson’s ratio.

The radial stress is continuous at the junction of elastoplastic zones, so when \(r = R_p, \sigma_r = \sigma_{re}\), the stresses in the plastic zone can be illustrated as follows:

\[
\sigma_o = k_{p2}\sigma_r + \sigma_{cp}
\]

3. Stresses in the residual zone

At the junction of the plastic zone and the broken zone, when \(r = R_s = \lambda R_p, \sigma_{cs} = \sigma_{ce}\). Equation (10) changes as follows:

\[
\sigma_{cs} = \sigma_{ce} + \beta M \left[ 1 - \frac{1}{\lambda^2} \right]
\]

\[\lambda = \sqrt{\frac{\beta M}{\sigma_{ce} - \sigma_{cs} + \beta M}}\]

where \(R_s\) is the radius of the broken zone, \(m\); \(\lambda\) is the radius ratio of the broken zone to the plastic zone, and \(\lambda = R_s/R_p\).

The residual strength expressed in Eqs. (14) and (5) is substituted into the equilibrium Eq. (6) and integrated, and the residual stresses can be obtained by combining the boundary conditions. The radial stress at the junction of the plastic zone and the residual zone is continuous, so the radial stress obtained by substituting \(r = R_s\) into Eq. (12) is taken as the boundary condition:

\[
\sigma_r = \left( \frac{2\sigma_o - \sigma_{ce} + \sigma_{ce} + \beta M}{k_{p1} + 1} + \frac{\beta M}{k_{p2} - 1} \right) \left( \frac{r}{R_p} \right)^{k_{p2} - 1} + \left( \frac{\beta M}{k_{p2} + 1} + \frac{\sigma_{ce} - \sigma_{ce} - \beta M}{k_{p2} - 1} \right) \left( \frac{r}{\lambda R_p} \right)^{k_{p2} - 1} - \frac{\sigma_{cs}}{k_{p2} - 1}
\]

\[
\sigma_o = k_{p2}\sigma_r + \sigma_{cs}
\]

**Thermal stress around the borehole**

In gas drilling, the heat transfer in the borehole is regarded as steady-state heat transfer, while the heat transfer in the formation outside the borehole is considered as unsteady-state heat transfer. Mathematical models of gas flow in drillstrings and annulus can be expressed by conservation equations of mass, momentum, and energy (Hasan et al. 1996a,b; Kabir et al. 1996; Keller et al. 1973; Lee 1982).
\[
\rho_gV_pA_p c_{pg} \frac{\partial T_p(z,t)}{\partial z} + 2\pi r_p U_i[T_p(z,t) - T_A(z,t)] = \rho_g V_p A_p c_{pg} \frac{\partial T_p(z,t)}{\partial t}
\]
\[
\rho_g V_A A_A c_{pg} \frac{\partial T_A(z,t)}{\partial z} + 2\pi r_p U_i[T_p(z,t) - T_A(z,t)] + \pi r_w h_1[T_w(z,t) - T_A(z,t)] = \rho_g V_A A_A c_{pg} \frac{\partial T_A(z,t)}{\partial t}
\]
where \(\rho_g\) and \(\rho_f\) are the density of gas and rock, kg/m\(^3\); \(V_p\) and \(V_A\) are the gas velocity in drillstrings and annulus, m/s; \(A_p\) and \(A_A\) are the cross-section of drillstrings and annular, m\(^2\); \(c_{pg}\) and \(c_{pg}\) are the specific heat of gas and rock, J/kg·°C; \(T_p, T_A,\) and \(T_w\) are the temperature of gas in drillstrings, gas in annulus, and rock in the borehole wall, °C; \(U_i\) is the total heat transfer coefficient between the drillstrings and the rock in the borehole wall, J/s·°C·m; \(h_i\) is the heat transfer coefficient of rock in borehole wall, J/s·°C·m; \(k_f\) is the formation thermal conductivity, J/h·°C·m; \(r, r_p,\) and \(r_w\) are the radial coordinates, drillstrings radius, and borehole radius, m; \(t\) is time, s; \(z\) is the well depth, m.

When gas is circulating in the gas drilling, the temperature around the borehole is changing and an additional thermal stress field is creating. The additional thermal stress around the borehole caused by the temperature difference can be obtained according to the heat conduction theory and thermoplastics mechanics (Nguyen et al. 2010).

\[
\sigma^T_r = - \frac{\alpha E}{(1 - \nu)} \frac{1}{r^2} \int_{r_w}^r T'(r,t) rdr - \alpha E T_w(t) \frac{r_w^2}{r^2}
\]

\[
\sigma^T_\theta = \frac{\alpha E}{(1 - \nu)} \frac{1}{r^2} \int_{r_w}^r T'(r,t) rdr - \alpha E T_w(t) \frac{r_w^2}{r^2}
\]
where \(\sigma^T_r\) and \(\sigma^T_\theta\) are the thermal stresses in the radial, tangential, and axial directions caused by formation temperature changes, MPa; \(\alpha\) is the thermal expansion coefficient of formation, 1/°C; \(T'(r,t) = T(r,t) - T_0, T_w(t) = T(r_w,t) - T(r_w,0)\) is the temperature distribution function of formation around borehole, \(T_w\) is the gas temperature at the borehole wall, °C. \(T_0\) is the initial formation temperature, °C.

**The radii of plastic zone and residual zone**

1. The radius of plastic zone

In gas drilling, both the original in situ stresses and thermal stress affect the surrounding rock deformation. It is the critical state that the plastic deformation is just complete, and the residual deformation does not occur yet. The radius of plastic zone at the critical state is \(R_{pc}\). The boundary conditions are \(r = r_w, \sigma_\varphi = \sigma_{pl}, \sigma_r = p_i\). Equation (10) is substituted into Eq. (12) and combined with Eq. (21), and the radius of plastic zone can be obtained as follows:

\[
R_{pc} = r_w \left( \frac{2\sigma_o - \sigma_{pl}}{k_p + 1} + \frac{2\beta M}{k_{p2} + 1} + \frac{\sigma_c}{k_{p2} - 1} \right)^{1/2}
\]
where \(R_{pc}\) is the critical radius of plastic zone, m; \(p_i\) is the gas pressure in borehole, MPa.

The radius of residual zone at the critical state is the borehole radius. The ratio of the residual and plastic zone is defined as \(\lambda = R/R_{pc}\), then \(\lambda = r_w/R_{pc}\), or \(R_{pc} = r_w/\lambda\) at the critical state. When the rock deformation around the borehole does not stop after it reaches the critical plastic zone, the residual zone will appear. The radius of residual zone will be greater than the borehole radius, that is, \(R \geq r_w,\) or \(R_{pc} \geq r_w/\lambda\). Therefore, comparison of the values of \(R_{pc}\) and \(r_w/\lambda\) can determine which stage of deformation appears in the surrounding borehole rock. Equation (11) can be expressed as follows according to the boundary condition: \(r = r_w\) and \(\sigma_r = p_i\).

\[
\left\{ \frac{2\sigma_o - \sigma_{pl}}{k_p + 1} + \frac{2\beta M}{k_{p2} + 1} + \frac{\sigma_c}{k_{p2} - 1} \right\} \left( \frac{r_w}{R_p} \right)^{k_{p2} - 1} - \frac{\sigma_c + \beta M}{k_{p2} - 1} - \frac{\beta M}{k_{p2} + 1} \left( \frac{R_p}{r_w} \right)^2 - p_i - \alpha E T_w(t) = 0
\]

In the range of \(R_{pc} \leq R \leq r_w/\lambda\), the radius of the plastic zone before the critical state can be gotten by the iterative solution of Eq. (24).

2. The radius of residual zone

When the rock around borehole reaches complete plastic deformation, the residual zone occurs, and its radius is greater than the borehole radius. The radius of residual zone can be illustrated by substituting the boundary condition of \(r = r_w\) and \(\sigma_r = p_i\) into Eq. (16).

\[
R_p = r_w \left( \frac{2\sigma_o - \sigma_{pl}}{k_p + 1} + \frac{\sigma_c + \beta M(1 - 2\omega^{k_{p2} - 1})}{(k_{p2} - 1)\omega^{k_{p2} - 1}} + \frac{\beta M(1 - 2\omega^{k_{p2} + 1})}{(k_{p2} + 1)\omega^{k_{p2} + 1}} \right)^{1/2}
\]
The universality of the model

The ideal elastic–plastic softening model can simplify two extreme cases: the ideal elastic–plastic model (a-b line in Fig. 1B) and the ideal fragility model (a-d-e line in Fig. 1B). Kastner’s formula of plastic zone radius is expressed according to the ideal elastic–plastic model. Airy’s formula for the radius of plastic zone is the extreme case according to the ideal fragility model.

1. The radius of plastic zone with the ideal elastic–plastic model

When the surrounding rock conforms to the elastic–plastic model, the fragility coefficient of rock $\beta = 0$, $k_{p1} = k_{p2} = k_p$. Without the influence of thermal stress, the radius of plastic zone can be simplified from Eq. (23) as follows:

$$ R_s = \lambda R_p $$

$$ R_p = r_w \left( \frac{\frac{2}{k_p+1} \left( \frac{\sigma_o + \sigma_{ce}}{k_p-1} \right)^{\frac{1}{k_p-1}}}{p_i + \frac{\sigma_{ce}}{k_p+1}} \right) $$

Equation (27) is the formula that Kastner proposed to calculate the radius of the plastic zone under the ideal elastic–plastic model (Kastner 1971).

2. The radius of plastic zone with the ideal elastic-brittle model

When the surrounding rock conforms to elastic-brittle model, the fragility coefficient of rock is $\beta \to \infty$, $k_{p1} = k_{p2} = k_p$. The limit of Eq. (15) can be calculated as $\lambda \to 1$. Without the influence of thermal stress, the limit analysis for both ends of Eq. (23) can obtain the radius of plastic zone:

$$ R_p = r_w \left( \frac{\frac{2\sigma_o}{k_p+1} + \frac{\sigma_{ce}}{k_p-1} - \frac{\sigma_o}{k_p+1}}{p_i + \frac{\sigma_{ce}}{k_p+1}} \right)^{\frac{1}{k_p-1}} $$

**Fig. 3** Measured radius of borehole and radius of bit in the gas drilling section
Equation (28) is the formula that Airy proposed to calculate the radius of plastic zone under the ideal elastic–plastic model (Yu et al. 1983).

Therefore, Kaster and Airy models for the radius of plastic zone can be obtained by simplifying the ideal elastic–plastic softening model proposed in the paper. The ideal elastic–plastic softening model has good universality.

Model validation

During gas drilling, the stability of the rock around borehole can be estimated by comparing the measured borehole radius with the plastic radius calculated by the model. The accuracy of the model can be verified indirectly if the variation trend of the plastic radius of surrounding rock is close to the measured borehole radius.

As an example, the data of the well HB021 in Xinjiang oilfield is used for validating the model. The gas drilling section of the well HB021 is the depth of 1000–2200 m, and the well radius curve is shown in Fig. 3 which shows that the radius of the well Sect. 1300–1600 m is seriously enlarged because the borehole wall collapse is severe. The borehole radius at the depth of 1000–1300 m is larger than other sections.

The construction and thermodynamic parameters of the well HB021 are listed in Table 1.

| Parameters                                      | Value  |
|-------------------------------------------------|--------|
| Upper hole diameter, mm                         | 311.2  |
| Casing O.D, mm                                  | 244.5  |
| Casing-wall thickness, mm                       | 8.94   |
| Casing setting depth, m                         | 1000   |
| Pipe O.D, mm                                    | 127    |
| Pipe I.D, mm                                    | 108.6  |
| Collar O.D, mm                                  | 158.25 |
| Collar I.D, mm                                  | 71.44  |
| Collar Length, m                                | 300    |
| Bit diameter, mm                                | 215.9  |
| Nozzle diameter, mm                             | 21     |
| Number of nozzles                               | 3      |
| Thermal conductivity of drillstrings and casing, W/m °C | 23.26 |
| Thermal conductivity of cement ring, W/m °C      | 0.52   |
| Formation thermal diffusion coefficient, m²/s   | 1.03   |
| Formation thermal conductivity, W/m. °C          | 2.06   |
| Thermal expansion coefficient of formation, 10⁻⁵/°C | 2.36   |
| Density of rock, kg/m³                          | 2540   |
| Young’s modulus of rock, GPa                    | 40     |
| Rock Poisson’s ratio                            | 0.2    |
| Rock cohesion, MPa                              | 14.08  |
| Internal friction angle of rock, degree         | 18.8   |
| Brittleness coefficient of rock                 | 1.0    |
| Maximum horizontal geostress, MPa/100 m         | 2.23   |
| Minimum horizontal geostress, MPa/100 m         | 1.82   |
| Overburden pressure, MPa/100 m                  | 2.24   |
| Effective geostress coefficient                 | 0.4    |
| Geothermal gradient, °C/m                       | 0.0226 |
| Ground temperature, °C                          | 25     |
| Outlet pressure, MPa                            | 0.1    |
| Gas injection pressure, MPa                     | 2.0–4.0|
| Gas injection temperature, °C                   | 38     |
| Gas injection rate, m³/min                      | 150–180|
| Penetration rate, m/hr                          | 6.4    |

According to the borehole pressure and temperature parameters in Figs. 4 and 5, the plastic and broken radius of the borehole deformation in presence or absence of thermal stress is demonstrated in Fig. 6.

In Fig. 6, the plastic radius of the borehole obtained from the complete strain–stress model accompanied by thermal stress during gas drilling has a high consistency with the ones in Fig. 3. On the contrary, the radius of
the plastic zone of surrounding rock without thermal stress shows that it is smaller at the top and larger at the bottom, and the radii of the plastic and residual zones increases rapidly in the depth of 1500 m through 2200 m. The results obtained from the complete strain–stress model without thermal stress are not consistent with the actual radius of borehole in Fig. 3. Therefore, the complete strain–stress model accompanied by thermal stress is verified availability to gas drilling.

**Results and discussion**

Comparison between Figs. 6 and 5 shows that the plastic radius without considering thermal stress is much higher than the one with thermal stress near the bottom borehole. The borehole temperature is far lower than the original geothermal value in Fig. 5. Thermal stress results from temperature differences before and after drilling into the formation shrinks the rocks and counteracted the expansion of rock due to the in situ stress. In the upper part of the borehole, the rock expanded by the thermal stress because the borehole temperature is higher than the formation temperature. The expanded rock aggravates the expansion of rock under the original in situ stress of the borehole. Therefore, thermal stress at the bottom of the borehole enhances the stability of the borehole, while thermal stress at the upper part of the borehole aggravates the instability of the borehole.

When the rock of the borehole wall is in the elastic stage, its stability is very strong. However, if the rock is in the plastic stage, it is in the transition stage from stability to instability. If rock of the borehole wall is in the residual area, it comes to the unstable stage. The gas flow pressure in the borehole is usually less than 3 MPa during gas drilling. It is too weak to support the borehole...
In addition, the high velocity in gas drilling washed the well wall more severely than mud drilling, so the radius of the borehole expanded further, and ultimately, the rock in the borehole wall reached a stable state.

In order to compare with the conventional borehole stability evaluation method of mud drilling, the borehole deformation is given in the form of collapse pressure. The collapse pressure distributions of borehole wall is calculated for the different penetrated depth of 1300 m, 1600 m, 2000 m, and 2200 m still base on the data of the well HB021. The results are shown in Fig. 7.

Figure 7 shows that the collapse pressure of borehole wall is changing and presents a trend of gradually increasing with the increase of gas drilling depth. The collapse pressure at about 1400 m was positive at 2200 m. The borehole wall is unstable due to the weak gas support ability. It is worth noting that the collapse pressure method can also describe the wellbore stability of gas drilling, but it is not intuitive to use the plastic radius and broken radius method.

**Conclusions**

1. The borehole instability mechanism of gas drilling is different from that of mud drilling. In gas drilling, the borehole wall rock still has a certain bearing capacity after reaching peak strength. The deformation of rock around borehole can be divided into elastic zone, plastic zone, and fracture zone using complete stress–strain model, which is more consistent with the stress–strain process of borehole wall rock.

2. Introducing the thermal stress into the complete stress–strain evaluation model of the borehole wall stability, the comparison of calculating the radii of plastic zone and broken zone of surrounding rock of borehole with measured caliper, the results show that the established model can better explain the gas drilling borehole wall instability mechanism, the radius of plastic zone and broken zone characterization of gas drilling borehole wall stability more intuitive.

![Temperature distribution in the gas drilling section](image-url)
3. In the gas drilling process, the borehole temperature is much lower than the original formation temperature near the bottom of the hole, and in the upper part of the borehole, the borehole temperature is higher than the formation temperature. Thermal stress has a significant effect on borehole stability. The thermal stress in the bottom borehole makes the rock shrink and offset the expansion of the original in situ stress on the surrounding rock, thus enhancing the stability of the borehole wall. The surrounding rock in the top borehole expands under the action of thermal stress, enhancing the expansion of the surrounding rock toward the borehole and aggravating the instability of the borehole wall.
Fig. 7 Collapse pressure distributions of the different penetrated depth

Nomenclature  

- $E$: The elastic modulus of elastic deformation, MPa;  
- $E_p$: The softening modulus of plastic softening deformation, MPa;  
- $M$: The plastic deformation modulus, MPa;  
- $\beta$: The fragility coefficient;  
- $\sigma_r$, $\sigma_\theta$: The tangential and radial stresses, MPa;  
- $\sigma_{cp}$: The uniaxial compressive strength in the process of elastic deformation, MPa;  
- $\varphi_e$: The angle of internal friction of elastic deformation, degree;  
- $\sigma_{cs}$: The uniaxial compressive strength of the residual deformation, MPa;  
- $\sigma_o$: The gradual increase of the average horizontal goestress, MPa;  
- $R_p$: The radius of the plastic zone, m;  
- $R_s$: The radius of the broken zone, m;  
- $\lambda$: The radius ratio of the broken zone to the plastic zone, $\lambda = R_s/R_p$;  
- $\rho_g$, $\rho_f$: The density of gas and rock, kg/m$^3$;  
- $V_p$, $V_A$: The gas velocity in drillstrings and annulus, m/s;  
- $A_p$, $A_A$: The cross-section of drillstrings and annular, m$^2$;  
- $c_{pg}$, $c_{pf}$: The specific heat of gas and rock, J/kg.℃;  
- $T_p$, $T_A$, $T_w$: The temperature of gas in drillstrings, gas in annulus and rock in the borehole wall, ℃;  
- $U$: The total heat transfer coefficient between the drillstrings and the rock in the borehole wall, J/s ℃ m;  
- $h$: The heat transfer coefficient of rock in borehole wall, J/s ℃ m;  
- $k$: The formation thermal conductivity, J/h ℃ m;  
- $r_p$, $r_w$: The radial coordinates, drillstrings radius and borehole radius, m;  
- $t$: Time, s;  
- $z$: The well depth, m;  
- $\sigma_r^T$, $\sigma_\theta^T$: The thermal stresses in the radial, tangential, and axial directions caused by formation temperature changes, MPa;  
- $a$: The thermal expansion coefficient of the formation, 1/℃;  
- $T_0$: The initial formation temperature, ℃;  
- $R_{pc}$: The plastic zone radius of the critical state, m;  
- $\rho$: The borehole gas pressure, MPa

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Declarations

Conflict of interest  
The authors declare no competing interests.

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