Unified Noise Reduction using Adaptive Radial Basis Function

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Abstract: The images captured by SAR and sonar are blurred and corrupted more by speckle noise and also other types of noise like Gaussian noise and salt & pepper noise. Denoising all types of noise to get perfect image is a vital challenge, earlier works on the same mode addressed with one filter for one noise, there is no one common or unified filter which can denoise all types of noise. Therefore in this paper, we have designed a filter which not only removes speckle noise, but also combination of other noises. Here IUNR (Intelligent Unified Noise Reduction) algorithm is proposed which is based on neural network called adaptive radial basis function acts as a unified filter for Denoising. Proposed method needs a single noisy image to train the adaptive radial basis function neural network to learn the correction of the noisy image. The Gaussian kernel function is applied to reconstruct the local disturbance appeared because of the noise. The proposed adaptive radial basis function network is compared with the fixed form which has fixed spread and the center value of kernel function. This method can correct the image suffered from different varieties of noises like speckle noise, salt & pepper noise and Gaussian noise separately or combination of noise. Various standard test images are considered for test purpose with different levels of noise density and performance of proposed algorithm is compared with adaptive wiener filter.

Index Terms: Adaptive radial basis function, adaptive wiener filter, Gaussian noise and speckle noise.

I. INTRODUCTION

Underwater images have poor quality due to low contrast, inhomogeneous lighting, blur and color diminishing. Designing a noise model for underwater images has become a challenging area of research. In the literature, there are several filters designed to remove noise from the underwater images. One filter works well for one type of noise but worst for another type of noise. Practically in most of the applications, the environment consists of the mixture of noise, so there is a need of a unified noise correction model which has ‘knowledge’ to remove the noise rather than correcting the pixels as according to statistical change appeared because of noise in the local region. For example in SAR images, along with speckle noise, there exists Gaussian noise as well as salt & pepper noise. In this regard, the artificial neural network can be considered as one of the best choices. In the earlier neural network models, denoising is done on different types of noise.

This paper proposed a unified approach for Denoising by not only removing speckle noise and Gaussian noise but also the mixed noise. Among the various possibilities under the artificial neural network, the radial basis function model is preferred because of its universal approximation capability with a simplified model of architecture. The adaptive approach is applied in defining the center as well as spreads of kernel function to make the learning better and faster.

II. RELATED WORK

In 1988, Broomhead[1], introduced the nonlinear network models like feedforward network models with the concepts of generalization and interpolation. It maps the n dimensional inputs to m dimensional outputs. This introduces a network model based on the curve fitting based on radial basis functions (RBF). In this approach a subset of weights are to be considered for optimization. This has an advantage of few hidden units. [2] Proposed a distinguished learning method for neural network using the orthogonal least square method. This algorithm constructs an adequate network by choosing RBF centers one by one randomly. This algorithm has been applied to two different signal processing applications. [3] Proposed CRBFN (complex radial basis function neural network) for low order digital channel equalization with an extra parameter to reduce nonlinear distortion. [4] Presented the concept of adaptive RBF which gives improved performance for less number of centers. [5] proposed the supervised learning based on the gradient descent training.[6] Presented an approach of radial basis function for nonlinear mapping from Rn to R by using conditional clustering or fuzzy clustering. [7] Proposed a reformulated radial basis function is used gradient descent training with supervised learning. [8] Presented the new learning strategy involving not only local optimization of variances of activation function but also global optimization called as interactive gradient learning method. [9] Developed a stochastic search learning algorithm which proved to be better algorithm than back propagation error learning for the recurring artificial neural network.[10] Proposed conditional c-means learning algorithm which gives a better performance than the unconditional C-means algorithm. [11] Proposed an improvement of the conjugate learning algorithm in terms of speed of convergence.[12] Here the performance of MLP (Multi Layer Perceptron) is compared with the other denoising methods like BM3D(Block matching 3D filtering), median filter and JPEG image compression algorithm. Hence MLP gave excellent results in comparison to other methods in denoising of salt & pepper noise, stripe noise and JPEG quantization artifacts. [13] Proposed the concept of clustering and gave the comparative analysis of different kernel function implemented on a different c-means algorithm like fuzzy, rough and intuitionistic fuzzy algorithms.[14] Proposed a
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III. RESEARCH METHOD: RADIAL BASIS FUNCTION NEURAL NETWORK (RBF-NN)

RBF network performs Non-Linear Transformation over an input vector and then fed for classification. By using such transformation; it is possible to converge linear non-separable problem to a linear separable problem. This RBF network model is similar to a K-nearest neighbor models. The main basic concept of this model is that a predicted target value of an item seems to be as other items that have close values of the predictor variables. RBF neurons are positioned in space by the predictor variables. These predictor variables have the same dimensions as space. Then Euclidian distance is calculated from the evaluated point to the center of each neuron and RBF (kernel function) is applied to the distance. This will calculate the weights (influence) for each neuron. Further, a neuron is from a point being evaluated the less influence it has. The radial function is so named since the radial distance is the function argument. The detailed structure of RBF neural network has an input layer, an output layer and hidden layer between the two. Input layer carries input and has the equal number of neurons as inputs. A hidden layer has one or more neurons each having a kernel function, for example, output of this hidden layer and Gaussian function will become weighted input to output layer neurons. The final output appeared as a sum of the inputs from the output layer neurons. The Gaussian function characteristics defined through two parameters the center ‘c’ and spread ‘r’. So, in the proposed form of architecture, there are three parameters which get the change in the learning process, the weights ‘w’ which is between the hidden nodes and output nodes, the center ‘C’ and spread ‘r’ of the kernel function.

A. Training and Need of Adaptiveness

In practice, the neural network considers supervised training method. Though a learning algorithm is defined, the network weights are so adjusted that the error between the actual and desired response is minimized with respect to some optimization criteria. After training, the interpolation is performed by the network in the output vector space. Hence the network achieves a non-linear mapping between the input and the output vector spaces. The architecture of the RBF NN consists of three layers: an input layer, an output layer and a hybrid layer between the two.

The output of RBFNN is calculated according to Eq(1).

\[ y_i = f_i(x) = \sum_{k=1}^{N} W_{ik} \phi_k(x, c_k) = \sum_{k=1}^{N} W_{ik} \phi_k \left( \| x - c_k \|_2 \right), \quad (1) \]

where \( x \in \mathbb{R}^{n \times 1} \) is defined as an input vector, \( \phi_k(\cdot) \) is a function from \( \mathbb{R}^n \) to \( \mathbb{R} \), \( \| . \|_2 \) indicates the Euclidean norm, \( W_{ik} \) are called as weights in the output layer, \( N \) is called as center which...
indicates the number of neurons in the hidden layer. For each neuron, the Euclidean distance between associated centers and the input to the network is computed. The neuron in a hidden layer gives output which is a nonlinear function of the distance. The weighted sum of these hidden layer outputs are calculated as the output of the network. The function is Gaussian and is given by Equation 2.

\[ \phi(x) = \exp\left(-\frac{x^2}{\sigma^2}\right) \]  

(2)

Where parameter \( \sigma \) is called as spread parameter which controls the “width” of RBF. The centers are the subset of input data which forms the input data subset. This data subset performs the sampling. In this Gaussian RBF, the spread parameter is set as follows.

\[ \sigma = \frac{d_{max}}{\sqrt{2}} \]  

(3)

The total number of centers is maximum Euclidean distance between the centers and \( k \). Using Equation 2. The RBF of a neuron in the middle layer which is denoted as the hidden layer is given by

\[ \phi(x, c_k) = \exp\left(-\frac{k}{d_{max}} \| x - c_k \|^2 \right) \]  

(4)

In conventional methods the centers are randomly sampled and measures standard deviation from the available Euclidean distance. Hence for a highly concentrated set with little variation, this approach is appropriate. The optimal values of centers and the corresponding standard deviations are provided to improve the performance. The important task is to train the parameters by updating each parameter depending on the error in the output. This updation is done by using the gradient mechanism for each iteration.

B. Adaptive RBF NN

In the fixed RBF NN or static RBF, only one parameter is adjustable i.e weight of the output layer. This approach is simple, in order to perform adequate sampling of the input but has a large number of centers from the input data set which in turn will generate a relatively very large network. In the proposed adaptive method, we can adjust all the three parameters weight, position of centers and width of RBF. Hence supervised training is not only done by the weights in the output layer but also done by the position of the centers and the spread parameter in the hidden layer for every processing units. Therefore defining the error cost function is the primary step as given in equation (5).

\[ J(n) = \frac{1}{2} [e(n)]^2 = \frac{1}{2} \left[ y_d(n) - \sum_{k=1}^{N} w_k \phi(x(n), c_k(n)) \right]^2 \]  

(5)

With the RBF chosen as Gaussian, Equation 5 becomes

\[ J(n) = \frac{1}{2} \left[ y_d(n) - \sum_{k=1}^{N} w_k \exp\left(-\frac{\| x(n) - c_k \|^2}{\sigma_k^2(n)}\right) \right]^2 \]  

(6)

The updated equations for the weight, centers and spread are given by Equation 7, equation 8 and Equation 9.

\[ w(n+1) = w(n) + \mu_e \frac{\partial}{\partial w} J(n) \quad \gamma_{w=w(n)} \]  

(7)

\[ c_k(n+1) = c_k(n) + \mu_c \frac{\partial}{\partial c_k} J(n) \quad \gamma_{c=c_k(n)} \]  

(8)

\[ \sigma_k(n+1) = \sigma_k(n) - \mu_k \frac{\partial}{\partial \sigma_k} J(n) \quad \gamma_{\sigma=\sigma_k(n)} \]  

(9)

C. Algorithm: Adaptive RBFNN

Following are the steps for Adaptive RBFNN

1. The centers of RBF functions are selected from the set of input vectors.
2. The initial value of spread parameter for the RBF function is calculated.
3. Initialize Weights in the output layer to some small random values.
4. From the input vector, the network output is computed. according to equation 10

\[ \gamma(n) = \left[ \sum_{k=1}^{N} w_k \phi(x(n), c_k, \sigma_k) \right] \]  

(10)

5. Update the network parameters according to equation (11)

\[ w(n+1) = w(n) + \mu_e \delta(n) \eta \phi(n) \]  

(11)

\[ c_k(n+1) = c_k(n) + \mu_c \frac{\delta(n) \phi(x(n), c_k(n), \sigma_k^2(n))}{\sigma_k^2(n)} \]  

(12)

\[ \sigma_k(n+1) = \sigma_k(n) + \mu_\sigma \frac{\delta(n) \phi(x(n), c_k(n), \sigma_k^2(n))}{\sigma_k^2(n)} \]  

(13)

D. Functional Block Diagram

The proposed method has two phases, training phase and test phase as shown in functional block diagram Fig.1. In the phase of training, a noise-free image, and here SAR(Synthetic Aperture Radar) image is taken.

The steps involved in adaptive RBF based Denoising are:

1. Image Acquisition
2. Noise Insertion
3. Pre-Processing
4. Static RBF
5. Adaptive RBF
6. Performance comparison
7. Denoise image by ARBF
8. Performance comparison of ARBF and Adaptive Wiener Filter

First the underwater image is taken. It is made noisy by adding the salt & pepper noise to make the noisy image for the training purpose. In pre-processing, image pixel matrix is first normalized in the range of [0 1] by dividing each pixel value by the maximum value of pixel then, transform the normalized matrix into the number of blocks. Each block matrix is transformed into the vector which will appear as the input to the ARBF. The target for an input vector has taken from the set of training data.

A. SAR image is converted into a vector which forms corresponding spatial information in the vector which will appear as the input to the ARBF. The target for an input vector has taken from the set of training data. First the underwater image is taken. An adaptive form of learning is applied to recorrect the noise. Once learning is completed, the RBF parameters, weights, centers, and spread are stored which will be used to denoise the noisy image at
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To understand the benefits of proposed adaptiveness in the RBF in comparison to static RBF, learning the behavior of both networks with a noisy image have been considered for 5 different trials. SAR image with and without noise has been considered for training purpose. Noisy image after preprocessing is applied as the input and corresponding spatial information in the normal image is considered as the target. Observed mean square error (MSE) under different trials is shown in Table 1. It is observed that there is no proper learning with SRBF because, there were only output weights, which were changing to acquire the knowledge, hence it was difficult to minimize the error as the spatial information getting changed from one location to another. The variation of obtained final MSE with the same number of iterations is very large. This is because of change in the selection of centers and spread parameters value from one trial to another. Because of high error and high variation in the trial, SRBF is not an appropriate method for denoising. When the proposed form of adaptiveness is applied in the ARBF, the obtained performance under different trials as shown in the Table 1 is appealing (mean error: 0.3114). Under all trials, the learning convergence characteristics for SRBF and ARBF are as shown in Fig. 4. It is observed that there is very less change in the error for SRBF even after providing the number of iterations. While with ARBF there is a sharp decline in error value observed with iterations because of the change in the centers and spreads.

IV. RESULTS & DISCUSSIONS

To get the benefits with the developed method, SAR image (fish image) is taken. In order to compare the static RBF and the Adaptive RBF, first the image is made noisy by adding speckle noise with noise density of 0.2, as shown in Fig. 3. This image is trained for 5 iterations for training purpose. Both the, fixed RBF and Adaptive RBF are applied independently for 5 iterations. To get the information about consistency in the performance, experiment is repeated for 5 independent trials. Performance analysis is done based on mean square error. The experiment is performed on different grayscale images of size 512*512 pixels. Preprocessing is applied to each image in a normalized form and each image is divided as a block of 3*3 pixel. RBF neural network architecture contains 9 input nodes, 2 hidden nodes, and 9 output nodes. Weights have initialized as the random number by a uniform distribution in the range of [-0.5 0.5]. The mean error in learning of SRBF and ARBF is shown in Fig. 3 while their convergence characteristics for all trials have shown in Fig. 4. It is clear that there is a very high error in learning is observed with SRBF as compared to ARBF.

A. Simulation results of SRBF vs ARBF.
The comparison of static and adaptive RBF in the Fig.4 indicates that the convergence rate is faster in adaptive RBF than static RBF. The comparative performance of the proposed model of noise reduction using ARBF against Adaptive Weiner filter is shown in Table 3. It is observed that under various noise reduction measuring parameters, the proposed method has delivered the better performance. The direct quality measure through the PSNR, it is observed that there is more than 4db improvement using proposed method which is very significant value. To get the more clear picture of comparison in Fig.5 bar plot of PSNR is given between the noisy image, de-noised image by AWF and IUNR. To get the visual perception about the quality of noise reduction through the proposed IUNR, Fig.6 shows the simulated result of de-noised image.

Table 2: Performance analysis of Adaptive wiener filter and proposed IUNR

| Noise Characteristics       | Adaptive Wiener filter | IUNR      |
|-----------------------------|------------------------|-----------|
| Mean Noise Reduction        | 50.4727                | 46.9392   |
| Mean in Unnoised Information| 4.3925                 | 4.4049    |
| Std Dev in Unnoised Information| 11.2783               | 8.3384    |
| Signal to Noise Ratio       | 11.3300                | 11.4774   |
| Peak Signal to Noise Ratio  | 22.2118                | 23.1313   |

From the above Table 2, PSNR of image by Adaptive Wiener Filter is 22.21 whereas by proposed filter PSNR is improved to 23.13.

B. Simulation results of mixed noise model (speckle & gaussian noise)

Practically there is no environment filled with single characteristics of noise but it is a mixture of different types of noise. Hence appropriate modeling of existing noise is very difficult to make. In such case application of the dedicated filter for a particular noise, model degrades the performance further. The proposed IUNR method has the capability to reconstruct the image even it suffered from different types of noise. In Fig.7, boat image is shown with a mixture of noise with Gaussian and Speckle noise. It can be observed that available noise has destroyed the valuable information of the original image. When the noisy image corrected with AWF and IUNR the obtained performance has shown in Table 4. It is observed that as in the case single noise model, with the mixed noise model, IUNR performance is superior in comparison to AWF. In Fig.8 the learning characteristics of ADRF has shown for 5 iterations. The denoised image has shown in Fig.9 and observed that that information which was nearly impossible to visualize in a noisy image, after denoising it is easy to find out.
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From the above table 4, PSNR of noisy image is 12.78, PSNR of image by Adaptive Wiener Filter is 19.78 and that of proposed ARBF is 20.58. It is observed that the PSNR of proposed algorithm is improved in comparison with adaptive wiener filter.

![Figure 7: Original image and noisy image (mix of Gaussian and speckle noise)](image)

![Figure 8: Convergence characteristics for ARBF](image)

![Figure 9: Simulation result of original, noisy image and ARBF denoised image](image)

| Noise Characteristics | Adaptive Wiener Filter | Proposed Adaptive RBF |
|-----------------------|------------------------|------------------------|
| Mean Noise Reduction  | 57.3831                | 60.6994                |
| Mean in Unnoised Information | 15.3673                | 11.9365                |
| Std Dev in Unnoised Information | 18.2839                | 14.4999                |
| Signal to Noise Ratio | 14.3378                | 14.4844                |
| Peak Signal to Noise ratio | 19.2813                | 20.5827                |

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