Cooperative virus propagation underlies COVID-19 transmission dynamics

Ziwei Dai¹ and Jason W. Locasale¹,²

¹ Department of Pharmacology and Cancer Biology, Duke University School of Medicine, Durham NC 27710 USA
² Department of Molecular and Structural Biochemistry, North Carolina State University, Raleigh NC 27607

Correspondence: Jason Locasale dr.jason.locasale@gmail.com or Ziwei Dai ziwei.dai@duke.edu

Abstract

The global pandemic due to the emergence of a novel coronavirus (COVID-19) is a threat to the future health of humanity. There remains an urgent need to understand its transmission characteristics and design effective interventions to mitigate its spread. In this study, we define a non-linear (known in biochemistry models as allostERIC or cooperative) relationship between viral shedding, viral dose and COVID-19 infection propagation. We develop a mathematical model of the dynamics of COVID-19 to link quantitative features of viral shedding, human exposure and transmission in nine countries impacted by the ongoing COVID-19 pandemic. The model was then used to evaluate the efficacy of interventions against virus transmission. We found that cooperativity was important to capture country-specific transmission dynamics and leads to resistance to mitigating transmission in mild or moderate interventions. The behaviors of the model emphasize that strict interventions greatly limiting both virus shedding and human exposure are indispensable to achieving effective containment of COVID-19.
Introduction

A novel disease (COVID-19)\(^1\)-\(^3\), which was first detected in December 2019 and then found to be caused by a newly discovered coronavirus, severe acute respiratory syndrome coronavirus-2 (SARS-CoV-2), has become a global pandemic, causing millions of infections, and claiming more than 240,000 lives as of the time of this publication. In response to the outbreak of COVID-19, China launched extremely aggressive, unprecedented actions including social distancing measures, school and workplace closures, travel bans, centralized quarantine of infected individuals, and contact tracing using cell phone tracking. While new infections and deaths have been greatly reduced in China\(^4\)-\(^6\) and in some other countries, the disease is rapidly spreading in many countries, among which the United States, with mixed efforts to limit transmission, has suffered from the highest number of confirmed cases and deaths. It speaks for itself the importance and urgency of understanding what interventions may best serve public health. A knowledge about the underlying mechanisms governing virus transmission dynamics gives insight into this question.

Mathematical models have been used to understand the transmission dynamics of epidemics\(^7\) from seasonal influenza\(^8\) to the Ebola virus\(^9\), forecast their outbreak and spread, and evaluate the efficiency of interventions in containing these diseases\(^10\). The most widely applied mathematical models in epidemiology are compartmental models, for instance, the susceptible-infected-recovered-deceased (SIRD) model, in which the total population is divided into several categories susceptible, infected, recovered, and deceased, between which exchange occurs. These models have served a fundamental role in reaching a quantitative understanding of transmission...
characteristics of COVID-19, such as estimation of basic reproduction number (R₀), incubation period, and fatality rate\textsuperscript{11-15}, and evaluation of the efficacies of interventions\textsuperscript{5,6,16-19}. While these models have greatly contributed to our current understanding of the COVID-19 pandemic, they lack information on infection mechanisms by SARS-CoV-2 and overlook the quantitative relationship between the rate of infection and dose of viral exposure. Instead, spread of the disease is taken to be directly mediated by interactions between infected and susceptible individuals, which are assumed to occur through linear relationships, thus creating a gap between the modeling tools currently available and the knowledge about detailed parameters of the virus, such as rates of virus shedding and decay\textsuperscript{20,21}, source-dependent viral dose\textsuperscript{22,23}, and dose dependent infectivity\textsuperscript{24}, for which experimental data have been collected but not yet used in the development of quantitative models of the pandemic\textsuperscript{25}.

Here, we develop a novel mathematical model for the transmission dynamics of COVID-19. We show that the cooperativity in infection between uninfected and infected individuals is critical in explaining the transmission dynamics of COVID-19 in countries most severely impacted by the pandemic. Cooperativity has a long history in the study of biological dynamics that began with models of ligand binding to receptors with multiple binding sites and has numerous applications to understand fundamental molecular processes in living cells such as gene transcription and signal transduction\textsuperscript{26,27}. Despite the complexity in the pathology of diseases such as COVID-19, there exists a mechanistic similarity between the binding of a ligand and activation of a receptor with multiple binding sites, and the release of virus from an infected person and transmission to an uninfected host. Preliminary studies on the dose-dependent
response to virus infection have also demonstrated that the relationship between viral exposure and infection is non-linear, suggesting that the infection kinetics is more complicated than assumed in the original epidemic models. Thus, consideration of this cooperativity may offer novel insights about how the virus is transmitted and how the pandemic can be effectively controlled.

Results

A cooperative infection model captures country-specific COVID-19 transmission dynamics

To incorporate viral dose and cooperative infection into compartmental infectious disease models, we introduced a variable $V$ quantifying the abundance of the virus to a reduced SIRD model in which the total number of recovered (R) and deceased (D) people are treated as a single variable, non-susceptible (N) population (Figure 1A, Methods). The reason for using a reduced model instead of the original SIRD model is that the rates for the transition from infected (I) to recovered (R) and deceased (D) are both proportional to the number of infected individuals (I), thus the sum of these two, N, also changes with a rate proportional to I. Moreover, a model with fewer parameters has the advantage of reducing parameter uncertainty and better avoiding overfitting. Using a standard mathematical term describing the cooperative relationship between $V$ and infection of susceptible individuals by viable virus particles, we derived three variations of the original SIRD model, including the reduced SIRD model, the reduced SIRD model with virus pool, and the reduced SIRD model with virus pool and cooperative infection (Figure 1A, Methods). Cooperativity was modeled using a Hill function with two parameters accounting for
the levels of cooperativity and saturation in response to viral dose, respectively (Methods). These models were then compared as to their accuracy in fitting data consisting of COVID-19 case numbers, recovered and deceased individuals in the nine countries with the highest and still rapidly increasing numbers of COVID-19 infections and deaths, which indicate ongoing COVID-19 pandemic as of Apr 3, 2020. These countries include USA, Turkey, UK, Spain, Italy, Germany, France, Switzerland, and Iran. Accuracy of fit was determined by a cost function defined as the mean squared deviation between simulated and actual daily numbers of infected individuals and non-susceptible individuals on dates within the time window between the confirmation of the first infection in the country and Apr 3, 2020 (Figure 1B). We found that among the three models, the reduced SIRD model with a virus pool and cooperative infection (i.e. the cooperative infection model) reached higher accuracy compared to the other two models in all countries, and was able to generate satisfactory fitting (i.e. optimal cost function < 0.005, which means that the mean error for each data point is less than 7.07% of the maximal value of actual data over the entire time course) in 7 out of the 9 countries (Figure 1C). By contrast, the two models without cooperative infection generated satisfactory fitting in only two countries, and the addition of the virus pool to the reduced SIRD model did not increase the fitting accuracy of the model despite the increased complexity of model (absolute difference in $-\log_{10}(\text{Optimal value of cost function})$ smaller than 0.003 for all countries, Figure 1C), suggesting that consideration of cooperativity in infection is critical for the model to accurately predict the COVID-19 transmission dynamics. The cooperative infection model also includes parameters directly related to other factors contributing to the viral dose dynamics, such as rate
constants for virus shedding and decay, and parameters quantifying the overall susceptibility of healthy population to the virus and efficiency of patient clearance (Figure 1D). Inference of these parameters from COVID-19 transmission data in different countries would offer valuable insights into the intrinsic properties of the virus and its specific transmission characteristics in each country.

The cooperative infection model predicts country-specific COVID-19 transmission dynamics

To predict COVID-19 transmission dynamics in the seven countries where the cooperative infection model was consistent with its previous transmission dynamics, we simulated the model over a time window of 80 days starting from February 15, 2020 with parameter sets that satisfactorily fit the data for each country. Parameter sets generating satisfactory fits were obtained by sampling the parameter space (Methods). We found that, in the absence of intervention, all seven countries were predicted to undergo significant increase in the number of infected individuals, especially for the countries UK, USA and Turkey, for which the numbers of infections were predicted to increase rapidly without any tendency of slowdown (Figure 2A, Supplementary Figure 1). To understand COVID-19 transmission characteristics in different countries, especially those predicted to face more future challenges, we examined distributions of parameters determining the transmission dynamics in each country (Figure 2B). We found that the two model parameters that significantly differ across countries are related to the susceptibility of the healthy population to infection (k) and the efficiency of patient clearance (a), while
parameters quantifying viral dose dynamics (c and d) and the cooperativity in response to viral
dose (n and K) showed no difference between countries (Figure 2B). These results further
support the use of the cooperative infection model because parameters for virus shedding, decay
and dose response are directly determined by intrinsic properties of the virus\(^20\), thus we expect
values of these parameters to be indistinguishable between countries, while the susceptibility of
the healthy population and efficiency of patient clearance reflects the performance of public
health measures and the healthcare systems which are country-specific. Notably, USA, UK and
Turkey are the three countries with lowest efficiency of patient clearance among the seven
countries, while the USA population was also found to suffer from the highest susceptibility to
infection.

**Extremely strict interventions are needed to control the COVID-19 pandemic**

We next assessed efficiency of different intervention strategies by simulating their influences on
model-predicted disease transmission dynamics. We considered two scenarios of intervention:
the infected individual-based intervention that targets the infected population to reduce virus
shedding from the infected individuals, and the population-based intervention that limits both
virus shedding from infected individuals and exposure of susceptible individuals to the virus.
The two scenarios of intervention were modeled by introducing a coefficient \(\alpha\) that quantifies
the strength of intervention, to the cooperative infection model (Figure 3A). We considered three
different levels of intervention strength (Figure 3B), equivalent to the approximate efficiency of
N95 respirators (\(\alpha = 0.1\)), surgical masks (\(\alpha = 0.2\)), and homemade masks (\(\alpha = 0.5\))\(^{28-30}\).
Assuming that the intervention starts at 48 days after the onset of the pandemic in the country (i.e. the date when the first COVID-19 case in the corresponding country was confirmed), we simulated the infection dynamics over a time window of 100 days starting from the onset of pandemic (Figure 3C, Supplementary Figure 2) and computed the relative number of infected individuals 100 days after the onset (Figure 3D). Notably, we found that only population-based interventions with extremely high intervention strength ($\alpha = 0.1$, equivalent to all people wearing N95 respirators) were sufficient to effectively prevent the growth of infected population (number of infected individuals on day 100 $< 15\%$ of the number in the absence of interventions for all countries except for Turkey and 39.8% for Turkey, Figure 3D). Taken together, these results suggest that in response to the COVID-19 pandemic, extremely strict interventions that affect the entire population are indispensable to prevent the spread of the disease.

**Cooperative infection results in resistance to public health interventions**

To understand how inclusion of the cooperative infection term contributes to the response of COVID-19 transmission dynamics to interventions, we next examined how the cooperative infection term $H$, which determines the rate of infection together with the susceptibility of healthy population and number of susceptible individuals (Figure 4A), depends on the dose of viable virus. For each country, we simulated the relationship between the viral dose and the cooperative infection term using 5,000 parameter sets (Figure 4B). We found that, compared to a linear relationship, the cooperative infection term $H$ has the tendency of amplifying a relatively small concentrations of virus, resulting in higher sensitivity to lower viral doses (i.e. small
amount of virus is able to cause a considerable number of infections) and stronger resistance to a reduction in viral dose (i.e. moderate reduction in viral dose is insufficient to effectively prevent the infections). We further illustrate this feature of the cooperative infection model by simulating the influence of different levels of viral concentration reduction on the value of cooperative infection term (Figure 4C). We found that, under a moderate-to-strong intervention that reduces the viral concentration by 90% (the left panel), the value of the cooperative infection term was only reduced by around 40% to 70% (values ranging from 44.9% for Germany to 68.6% for UK based on parameters with optimal fitting, left panel of Figure 4C, yellow stars). This finding indicates that the majority of infections cannot be prevented by these interventions. On the other hand, under an extremely strong intervention that removes 99% of the virus (the right panel), the value of cooperative infection term was effectively reduced by the extent of more than 90% (values ranging from 93.0% for Italy and 97.3% for France, right panel of Figure 4C, yellow stars). Taken together, these results demonstrate that the cooperativity in infection, which has been found to be indispensable for the model to accurately reproduce country-specific COVID-19 transmission dynamics in our previous analysis, dampens the effects of interventions, thus requiring extremely strong interventions to effectively mitigate the pandemic.

**Discussion**

In this study, we have developed a mathematical model for the transmission dynamics of COVID-19 based on the concept of cooperativity in biology. The model was found to accurately reproduce the transmission dynamics of COVID-19 in seven countries that are most severely
impacted by the pandemic while models without the cooperative infection were inconsistent with available data. These findings highlight the importance of cooperativity in shaping population level responses to an infectious virus and offer new insights into the transmission dynamics of infectious diseases. Notably, the cooperativity in infection leads to the resistance of virus transmission to intervention strategies that are not strong enough, resulting in increased difficulty in designing effective interventions to control the pandemic. Aggressive interventions with the strength approximately equivalent to at least requiring all individuals, no matter infected or not, to wear N95 respirators all time while in public space, are predicted to be necessary by the model. These findings together stress the necessity of strong interventions in effectively controlling the transmission of COVID-19.

We also note that, as with any mathematical model for a complicated process, this model is not without limitations. Like all models in computational epidemiology, this model does not account for many factors that contributes to the transmission of COVID-19. First, this model assumes that there is no regional heterogeneity and that the population is homogenously mixed, while it has been demonstrated that the susceptibility to and fatality of COVID-19 depends on many demographic factors, such as gender and age, and life style related variables, such as smoking history. Countries are assumed to be isolated from each other, which means no international travels occur during the time period, while imported cases likely contribute to many COVID-19 outbreaks around the world. Moreover, since a data-driven approach was used to parameterize the models, it might underestimate the severity of the pandemic because of the existence of undocumented infections due to the limitation of diagnostic capacity. Other factors
not included in the model, such as seasonality in transmission of coronaviruses\textsuperscript{14}, existence of asymptotic infections\textsuperscript{34}, and change of case definition\textsuperscript{35} may also affect the epidemic curve of COVID-19. Nevertheless, the model, while possibly underestimating the severity of COVID-19 due to simplification, still forecasts the rapid escalation in COVID-19 spread, and highlights the extreme urgency of stronger interventions such as contact tracing, rigorous social distancing, or the application of N95 respirators for public use by showing that moderate interventions are not likely to effectively reduce transmission due to the cooperative infection term. Modest measures such as those adopted so far in the USA unfortunately nevertheless disrupt the normal function of society and creates substantial economic and societal costs and may not be effective as planned.

In summary, this study develops a cooperative infection model that connects viral dynamics to the transmission dynamics of COVID-19 at the population level, captures the nonlinearity in the dose-response relationship in viral infection, correctly reproduces COVID-19 transmission characteristics in different countries, and, forecasts the rapid spread of COVID-19 in the absence of extremely strong interventions due to the cooperativity in SARS-CoV-2 infection. While further research and analysis are needed to improve the model and better understand the molecular mechanisms behind the cooperativity in viral infection, the predictions of this model demonstrate the indispensability of stronger interventions\textsuperscript{14,36} that should encourage policy makers with interests in public good.

**Data and code availability**

Data and code used in this study are available at the GitHub page of the Locasale Lab:
https://github.com/LocasaleLab/COVID_19_models.

Acknowledgments

JWL thanks the Marc Lustgarten Foundation, the National Institutes of Health (R01CA193256) and the American Cancer Society (129832-RSG-16-214-01-TBE) for their generous support.

Figure legends

Figure 1. A cooperative infection model captures country-specific COVID-19 transmission dynamics

A. Diagrams of the original SIRD model, reduced SIRD model, reduced SIRD model with virus pool, and reduced SIRD model with virus pool and cooperative infection.

B. Workflow for the model selection process and the definition of cost function used.

C. Optimal cost function values achieved in fitting country-specific COVID-19 transmission data using the reduced SIRD model, reduced SIRD model with virus pool, and reduced SIRD model with virus pool and cooperative infection. The dashed horizontal line indicates the threshold of cost function value for satisfactory fitting. A parameter set with cost function value lower than this threshold was considered satisfactory.

D. Equations for the reduced SIRD model with virus pool and cooperative infection and meaning of model parameters.

Figure 2. The cooperative infection model predicts country-specific transmission dynamics
A. Model-predicted numbers of infected individual during the time window of 80 days starting from February 15, 2020 and comparison between model-predictions and actual data for dates before April 3, 2020.

B. Range of country-specific model parameters estimated from fitting the COVID-19 transmission data by country.

**Figure 3. Extremely strict interventions are needed to control the COVID-19 pandemic**

A. Diagram and model equations for the cooperative infection model under infected individual-based intervention (upper panel) and population-based intervention (lower panel).

B. Values of the intervention strength coefficient $\alpha$ used in simulation of the interventions and their equivalent levels of virus-blocking efficiency.

C. Model-predicted numbers of infected individuals before and after the intervention for both infected individual-based and population-based interventions under different intervention strengths. Shaded regions were computed from simulations based on 5,000 randomly sampled parameter sets that satisfactorily fit the country-specific transmission data.

D. Relative numbers of infected individuals under interventions on day 100 since the onset of pandemic compared to the case without intervention. Values for each country were computed based on the parameter set with optimal fitting for that country.

**Figure 4. Cooperative infection results in resistance to public health interventions**

A. Definition of the cooperative infection term and its relationship with the rate of infection.
B. Relationship between viral dose and value of the cooperative infection term in different countries.

C. Influence of reducing the viral dose by 90% (left panel) or 99% (right panel) on the value of cooperative infection term. Violin plots were drawn based on distribution of the relative cooperative infection term values computed from 5,000 randomly sampled parameter sets. Circles indicate median values based on the 5,000 simulations and stars indicate values computed based on parameter sets with optimal fitting.

References

1. Wu, F. et al. A new coronavirus associated with human respiratory disease in China. *Nature* **579**, 265-269, doi:10.1038/s41586-020-00208-3 (2020).
2. Zhou, P. et al. A pneumonia outbreak associated with a new coronavirus of probable bat origin. *Nature* **579**, 270-273, doi:10.1038/s41586-020-0127-0 (2020).
3. Zhu, N. et al. A Novel Coronavirus from Patients with Pneumonia in China, 2019. *N Engl J Med* **382**, 727-733, doi:10.1056/NEJMoa2001017 (2020).
4. Maier, B. F. & Brockmann, D. Effective containment explains subexponential growth in recent confirmed COVID-19 cases in China. *Science*, doi:10.1126/science.abb4557 (2020).
5. Tian, H. et al. An investigation of transmission control measures during the first 50 days of the COVID-19 epidemic in China. *Science*, doi:10.1126/science.abb6105 (2020).
6. Zhang, J. et al. Changes in contact patterns shape the dynamics of the COVID-19 outbreak in China. *Science*, doi:10.1126/science.abb8001 (2020).
7. Hethcote, H. W. The mathematics of infectious diseases. *Siam Rev* **42**, 599-653, doi:10.1137/S0036144500371907 (2000).
8. Hill, E. M., Petrou, S., de Lusignan, S., Yonova, I. & Keeling, M. J. Seasonal influenza: Modelling approaches to capture immunity propagation. *Plos Computational Biology* **15**, doi:ARTN e1007096 10.1371/journal.pcbi.1007096 (2019).
9. Chretien, J. P., Riley, S. & George, D. B. Mathematical modeling of the West Africa Ebola epidemic. *Elife* **4**, doi:ARTN e09186 10.7554/eLife.09186 (2015).
10. Lin, F., Muthuraman, K. & Lawley, M. An optimal control theory approach to non-
pharmaceutical interventions. *Bmc Infect Dis* 10, doi:Artn 32 10.1186/1471-2334-10-32 (2010).

11 Wu, J. T. *et al.* Estimating clinical severity of COVID-19 from the transmission dynamics in Wuhan, China. *Nat Med*, doi:10.1038/s41591-020-0822-7 (2020).

12 Kucharski, A. J. *et al.* Early dynamics of transmission and control of COVID-19: a mathematical modelling study. *Lancet Infect Dis*, doi:10.1016/S1473-3099(20)30144-4 (2020).

13 Li, Q. *et al.* Early Transmission Dynamics in Wuhan, China, of Novel Coronavirus-Infected Pneumonia. *N Engl J Med* 382, 1199-1207, doi:10.1056/NEJMoa2001316 (2020).

14 Kissler, S. M., Tedijanto, C., Goldstein, E., Grad, Y. H. & Lipsitch, M. Projecting the transmission dynamics of SARS-CoV-2 through the postpandemic period. *Science*, doi:10.1126/science.abb5793 (2020).

15 Wu, J. T., Leung, K. & Leung, G. M. Nowcasting and forecasting the potential domestic and international spread of the 2019-nCoV outbreak originating in Wuhan, China: a modelling study. *Lancet* 395, 689-697, doi:10.1016/S0140-6736(20)30260-9 (2020).

16 Ferretti, L. *et al.* Quantifying SARS-CoV-2 transmission suggests epidemic control with digital contact tracing. *Science*, doi:10.1126/science.abb6936 (2020).

17 Kraemer, M. U. G. *et al.* The effect of human mobility and control measures on the COVID-19 epidemic in China. *Science*, doi:10.1126/science.abb4218 (2020).

18 Prem, K. *et al.* The effect of control strategies to reduce social mixing on outcomes of the COVID-19 epidemic in Wuhan, China: a modelling study. *Lancet Public Health*, doi:10.1016/S2468-2667(20)30073-6 (2020).

19 Giordano, G. *et al.* Modelling the COVID-19 epidemic and implementation of population-wide interventions in Italy. *Nat Med*, doi:10.1038/s41591-020-0883-7 (2020).

20 van Doremalen, N. *et al.* Aerosol and Surface Stability of SARS-CoV-2 as Compared with SARS-CoV-1. *N Engl J Med* 382, 1564-1567, doi:10.1056/NEJMc2004973 (2020).

21 He, X. *et al.* Temporal dynamics in viral shedding and transmissibility of COVID-19. *Nat Med*, doi:10.1038/s41591-020-0869-5 (2020).

22 Ong, S. W. X. *et al.* Air, Surface Environmental, and Personal Protective Equipment Contamination by Severe Acute Respiratory Syndrome Coronavirus 2 (SARS-CoV-2) From a Symptomatic Patient. *JAMA*, doi:10.1001/jama.2020.3227 (2020).

23 Liu, Y. *et al.* Aerodynamic analysis of SARS-CoV-2 in two Wuhan hospitals. *Nature*, doi:10.1038/s41586-020-2271-3 (2020).

24 Lunn, T. J. *et al.* Dose-response and transmission: the nexus between reservoir hosts, environment and recipient hosts. *Philos T R Soc B* 374, doi:ARTN 20190016 10.1098/rstb.2019.0016 (2019).

25 Bar-On, Y. M., Flamholz, A., Phillips, R. & Milo, R. SARS-CoV-2 (COVID-19) by the numbers. *Elife* 9, doi:10.7554/eLife.57309 (2020).

26 Monod, J., Wyman, J. & Changeux, J. P. On the Nature of Allosteric Transitions: A Plausible Model. *J Mol Biol* 12, 88-118, doi:10.1016/s0022-2836(65)80285-6 (1965).
Changeux, J. P. Allostery and the Monod-Wyman-Changeux Model After 50 Years. *Annu Rev Biophys* **41**, 103-133, doi:10.1146/annurev-biophys-050511-102222 (2012).

Balazy, A. *et al.* Do N95 respirators provide 95% protection level against airborne viruses, and how adequate are surgical masks? *Am J Infect Control* **34**, 51-57, doi:10.1016/j.ajic.2005.08.018 (2006).

Davies, A. *et al.* Testing the efficacy of homemade masks: would they protect in an influenza pandemic? *Disaster Med Public Health Prep* **7**, 413-418, doi:10.1017/dmp.2013.43 (2013).

Makison Booth, C., Clayton, M., Crook, B. & Gawn, J. M. Effectiveness of surgical masks against influenza bioaerosols. *J Hosp Infect* **84**, 22-26, doi:10.1016/j.jhin.2013.02.007 (2013).

Richardson, S. *et al.* Presenting Characteristics, Comorbidities, and Outcomes Among 5700 Patients Hospitalized With COVID-19 in the New York City Area. *JAMA*, doi:10.1001/jama.2020.6775 (2020).

Guan, W. J. *et al.* Clinical Characteristics of Coronavirus Disease 2019 in China. *N Engl J Med*, doi:10.1056/NEJMoa2002032 (2020).

Li, R. *et al.* Substantial undocumented infection facilitates the rapid dissemination of novel coronavirus (SARS-CoV2). *Science*, doi:10.1126/science.abb3221 (2020).

Gostic, K., Gomez, A. C., Mummah, R. O., Kucharski, A. J. & Lloyd-Smith, J. O. Estimated effectiveness of symptom and risk screening to prevent the spread of COVID-19. *Elife* **9**, doi:10.7554/eLife.55570 (2020).

Tsang, T. K. *et al.* Effect of changing case definitions for COVID-19 on the epidemic curve and transmission parameters in mainland China: a modelling study. *The Lancet Public Health*, doi:10.1016/S2468-2667(20)30089-X (2020).

Koo, J. R. *et al.* Interventions to mitigate early spread of SARS-CoV-2 in Singapore: a modelling study. *Lancet Infect Dis*, doi:10.1016/S1473-3099(20)30162-6 (2020).
Figure 1. A cooperative infection model captures country-specific COVID-19 transmission dynamics

A. Virus pool (V)

Reduced SIRD model

Recovered (R) and deceased (D) as a single variable N (non-susceptible)

Original SIRD model

Reduced SIRD model with virus pool and cooperative infection

B. Model selection

COVID-19 transmission models

Data of COVID-19 cases, recoveries and deaths in 9 countries

Cost function

\[ f(p) = \frac{1}{2n} \sum_{i=1}^{n} \left( \frac{t_i(p) - t_{i,\text{max}}}{\text{max}_i} \right)^2 + \sum_{i=1}^{n} \left( \frac{N_i(p) - N_{i,\text{max}}}{\text{max}_i N_i} \right)^2 \]

C. -log10(Optimal value of cost function)

USA Turkey UK Spain Italy France Germany Switzerland Iran

D. Reduced SIRD model with virus pool and cooperative infection

\[
\begin{align*}
\frac{d[S]}{dt} &= -k \frac{[V]^n + k}{[S]} \\
\frac{d[I]}{dt} &= k \frac{[V]^n + k}{[S]} - a[I] \\
\frac{d[N]}{dt} &= a[I] \\
\frac{d[V]}{dt} &= c[i] - d[V]
\end{align*}
\]

| Parameter | Description                                      | Symbol |
|-----------|--------------------------------------------------|--------|
| k         | Susceptibility to infection                      |        |
| c         | Virus shedding                                   |        |
| a         | Patient clearance (i.e. recovery and death)     |        |
| d         | Virus decay                                      |        |
| n         | Cooperativity in infection                       |        |
| K         | Saturation in response to viral dose             |        |
Figure 2. The cooperative infection model predicts country-specific transmission dynamics

A
Model-predicted numbers of infected individuals

B
Model parameters estimated from fitting COVID-19 transmission data by country
Figure 3. Extremely strict interventions are needed to control the COVID-19 pandemic

A. Infected individual-based intervention

\[ \begin{align*}
\frac{d[S]}{dt} &= -k \frac{(V)^n}{[V]^n + K} [S] \\
\frac{d[I]}{dt} &= k \frac{(V)^n}{[V]^n + K} [S] - a[I] \\
\frac{d[N]}{dt} &= a[I] \\
\frac{d[V]}{dt} &= \alpha c[I] - d[V]
\end{align*} \]

\( \alpha < 1 \): intervention strength coefficient

B. Efficiency

| \( \alpha \) | Efficiency |
|----------------|-------------|
| 0.1            | N95 respirators |
| 0.2            | Surgical masks |
| 0.5            | Homemade masks |

C. Model-predictions in USA under different interventions

Infected individual-based

\[ \begin{align*}
\frac{d[S]}{dt} &= -k \frac{(V)^n}{[V]^n + K} [S] \\
\frac{d[I]}{dt} &= k \frac{(V)^n}{[V]^n + K} [S] - a[I] \\
\frac{d[N]}{dt} &= a[I] \\
\frac{d[V]}{dt} &= \alpha c[I] - d[V]
\end{align*} \]

Population-based

\[ \begin{align*}
\frac{d[S]}{dt} &= -k \frac{[V]^n}{[V]^n + K} [S] \\
\frac{d[I]}{dt} &= k \frac{[V]^n}{[V]^n + K} [S] - a[I] \\
\frac{d[N]}{dt} &= a[I] \\
\frac{d[V]}{dt} &= \alpha c[I] - d[V]
\end{align*} \]

D. Relative number of infected individuals on day 100 compared to no intervention

- All people wearing N95 respirators
- All people wearing surgical masks
- Only infected individuals wearing N95 respirators
- Only infected individuals wearing surgical masks
- All people wearing homemade masks
- Only infected individuals wearing homemade masks
Figure 4. Cooperative infection results in resistance to public health interventions

\[
\frac{d[S]}{dt} = -k \frac{[V]^n}{[V]^n + K}[S]
\]

\[
H = \frac{[V]^n}{[V]^n + K}: \text{Cooperative infection term}
\]

A

B

Relationship between viral concentration and extent of cooperative infection

C

Cooperative infection under different extents of viral concentration reduction
Supplementary Material for

Cooperative virus propagation underlies COVID-19 transmission dynamics

Ziwei Dai¹ and Jason W. Locasale¹,²

¹ Department of Pharmacology and Cancer Biology, Duke University School of Medicine, Durham NC 27710 USA

² Department of Molecular and Structural Biochemistry, North Carolina State University, Raleigh NC 27607

Correspondence: Jason Locasale dr.jason.locasale@gmail.com or Ziwei Dai ziwei.dai@duke.edu

Methods

Data acquisition

Time-course data for numbers of currently infected individuals (i.e. active cases) and total infected individuals (i.e. total cases, including both infected individuals and recovered or deceased individuals) in the nine countries, which were used in fitting the models, were retrieved from https://www.worldometers.info/coronavirus/. Data for total population estimates in the nine countries, which were used in estimation of the initial number of susceptible people at the onset of pandemic in each country, were obtained from the 2019 Revision of World Population Prospects (https://population.un.org/wpp/).

Mathematical models for COVID-19 transmission

We develop our models based on the original SIRD model for transmission of an infectious disease:
\[
\begin{aligned}
\frac{d[S]}{dt} &= -b[S][I] \\
\frac{d[I]}{dt} &= b[S][I] - \gamma[I] - \tau[I] \\
\frac{d[R]}{dt} &= \gamma[I] \\
\frac{d[D]}{dt} &= \tau[I]
\end{aligned}
\]

In which \([S]\) is the total number of susceptible individuals, \([I]\) is the total number of infected individuals, \([R]\) is the total number of recovered individuals and \([D]\) is the total number of deceased individuals, \(b, \gamma\) and \(\tau\) are model parameters. To simplify this model, we let \([N] = [R] + [D]\) denote the total number of non-susceptible (i.e. recovered or deceased) individuals.

By letting \(a = \gamma + \tau\), we can then derive the equations describing the dynamics of the reduced SIRD model:

\[
\begin{aligned}
\frac{d[S]}{dt} &= -b[S][I] \\
\frac{d[I]}{dt} &= b[S][I] - a[I] \\
\frac{d[N]}{dt} &= a[I]
\end{aligned}
\]

Based on the reduced SIRD model, we further include an additional term \([V]\) quantifying the total size of viable virus pool. Dynamics of this variable depend on virus shedding from infected individuals with a rate linear to the total number of infected individuals \([I]\), and virus decay with a rate proportional to \([V]\). In the absence of cooperative infection, we assume a linear relationship between the chance of a susceptible individual being infected and \([V]\), that is, the infection of susceptible individuals happens with a rate proportional to the product of \([V]\) and \([S]\). Thus, we have equations for the reduced SIRD model with virus pool:
Finally, to model the cooperativity in infection of an individual, we assume that the relationship between the chance of a susceptible individual being infected and the viable virus pool size $[V]$ follows a non-linear relationship described by a Hill function $\frac{[V]^n}{[V]^n + K}$. Thus, we have differential equations for the dynamics of the reduced SIRD model with virus pool and cooperative infection (i.e. the cooperative infection model):

$$\begin{align*}
\frac{d[S]}{dt} &= -k[V][S] \\
\frac{d[I]}{dt} &= k[V][S] - a[I] \\
\frac{d[N]}{dt} &= a[I] \\
\frac{d[V]}{dt} &= c[I] - d[V]
\end{align*}$$

**Simulation and parameter space sampling of the models**

Models were implemented with MATLAB scripts and solved using the function ode23s() for solving stiff ordinary differential equations. Model parameters for each country were estimated using differential simulated annealing, a global optimization algorithm that allows sampling of the parameter space\(^1\), by minimizing the cost function:

$$f(p) = \frac{1}{2n} \left( \sum_{t=1}^{t=n} \left( \frac{l_t(p) - l_t}{\max_l l_t} \right)^2 + \sum_{t=1}^{t=n} \left( \frac{N_t(p) - N_t}{\max N_t} \right)^2 \right)$$

In which $p$ is a set of parameters, $n$ is the total number of time points with available data,
\( I_t(p) \) is the number of infected individuals on the \( t \)-th day predicted by the model with parameter set \( p \), \( I_t \) is the actual number of infected individuals on the \( t \)-th day, \( N_t(p) \) is the number of non-susceptible individuals on the \( t \)-th day predicted by the model with parameter set \( p \), \( N_t \) is the actual number of non-susceptible individuals on the \( t \)-th day. A parameter set \( p \) is considered to generate a satisfactory fitting to the actual data if \( f(p) < 0.005 \). All parameter sets with satisfactory fitting to the data found during the sampling were kept for the following analysis. Parameters used for the differential simulated annealing algorithm were initial temperature \( \beta_0 = 10^{-6} \), maximal temperature \( \beta_{\text{max}} = 10^8 \), cooling rate = 1.03, Markov chain length \( m = 500 \).

**Simulation of interventions**

Simulation of interventions was performed over a time window of 100 days starting from the onset of the first infection in each country. For each country, simulation was done with 5,000 parameter sets randomly selected from all sampled parameter sets with satisfactory fitting to the country-specific COVID-19 transmission data. An intervention was assumed to start on day 48. We first simulated the model without intervention in the time window of day 0 to day 48, and then simulated the model under the intervention from day 48 to day 100. For a parameter set \( p \), the relative number of infected individuals on day 100 under an intervention \( I \) was calculated as below:

\[
n_t(p) = \frac{N_t(p)}{N_0(p)}
\]

In which \( N_t(p) \) is the number of infected individuals on day 100 with the parameter set \( p \) and under the intervention \( I \), and \( N_0(p) \) is the number of infected individuals on day 100 with this
parameter set in the absence of intervention.

Simulation of the cooperative infection term

For each parameter set, we first simulated the cooperative infection model with that parameter set in the time span from the onset of the pandemic in the corresponding country to April 3, 2020, and recorded the maximal value of viral dose \([V], \max[V]\), during this time span. We then computed the values of the cooperative infection term \(H = \frac{[V]^n}{[V]^{n+K}}\) with the 101 values \([V] = 0, \frac{[V]_{\max}}{100}, \ldots, \frac{k\cdot[V]_{\max}}{100}, \ldots, [V]_{\max}\). Since \(H\) is a monotonically increasing function of \([V]\), we have the maximal value of \(H\) on the 101 \([V]\) values: \(H_{\max} = \frac{[V]_{\max}^n}{[V]_{\max}^{n+K}}\). Relative values of the cooperative infection term compared to \(H_{\max}\) were then plotted against the relative viral dose \(\frac{[V]}{[V]_{\max}}\) to illustrate the dependence of the cooperative infection term on viral dose.

Supplementary Figures

Figure S1. Model-predicted numbers of non-susceptible individuals
Figure S2. Model-predicted COVID-19 transmission dynamics under interventions

A  Model-predicted numbers of infected individuals under population-based intervention

B  Model-predicted number of infected individuals under infected individual-based intervention

References

1  Dai, Z. W. & Lai, L. H. Differential simulated annealing: a robust and efficient global optimization algorithm for parameter estimation of biological networks. *Mol Biosyst* 10, 1385-1392, doi:10.1039/c4mb00100a (2014).