Applicability of Aeroacoustic Scaling Laws of Leading Edge Serrations for Rotating Applications

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Abstract: The dominant aeroacoustic mechanisms of serrated leading edges, subjected to highly turbulent inflow conditions, can be compressed to spanwise decorrelation effects as well as effects of destructive interference. For single aerofoils, the resulting broadband noise reduction is known to follow spectral scaling laws. However, transferring serrated leading edges to rotating machinery, results in noise radiation patterns of significantly increased complexity, impeding to allocate the observed noise reduction to the underlying physical mechanisms. The current study aims at concatenating the scaling laws for stationary aerofoil and rotating-blade application and thus at providing valuable information on the aeroacoustic transferability of leading edge serrations. For the pursued approach, low-pressure axial fans are designed, obtaining identical serrated fan blade geometries than previously analyzed single aerofoils, hence allowing for direct comparison. Highly similar spectral noise reduction patterns are obtained for the broadband noise reduction of the serrated rotors, generally confirming the transferability and showing a scaling with the geometrical parameters of the serrations as well as the inflow conditions. Continuative analysis of the total noise reduction, however, constrains the applicability of the scaling laws to a specific operating range of the rotors and motivates for a devaluation of the scaling coefficients regarding additional rotor-specific effects.

Keywords: axial fans; rotating machinery; leading edge serrations; noise reduction; rotor-turbulence-interaction noise; aeroacoustics; aerodynamics

1. Introduction

For the single aerofoils under highly turbulent inflow conditions, the approaching turbulent structures cause pressure fluctuations that propagate as acoustic waves into the far-field [1], resulting in broadband noise radiation [2]. This broadband noise, mainly stemming from the leading edge of an aerofoil, can be drastically reduced by implementing a leading edge pattern of sinusoidal shape [3–5], called leading edge serrations. The general shape of these serrations is usually parametrized by the serration amplitude A and the serration wavelength λ (Figure 1), where the wavy shape of the serrations mainly results in three effects [6]. First, a cut-off of the acoustic sources along the oblique edges of the serrations [7–9], leading to weaker acoustic sources. Second, decorrelation effects [3,10] along the span of the aerofoil lead to reduced radiation due to phase differences. Eventually, the third effect can be attributed to destructive interference between the serration peak and the root region [3,7,11], leading to an extensive decrease of noise at frequencies where the acoustic wavelength corresponds to...
the size of the serration amplitude. A majority of the available studies concerning serrated leading edges were carried out based on single stationary aerofoils [4,7,12], even though the final application area is considered to be turbomachines, fans and blowers, or contra-rotating rotors, where only little research was carried out [13–15]. However, considering the acoustic sources of rotating machinery, it becomes apparent, that multiple additional noise sources are present (Figure 1). These include among others (a) effects in the blade tip region due to interaction of the rotating blades and the reverse flow, (b) noise due to secondary flows such as separated vortical structures interacting with subsequent blades, and (c) rotor–stator interaction noise. This already complex aeroacoustic pattern is bedevilled by radius-dependent inflow conditions of the blades in terms of the circumferential velocity (and turbulence conditions) as well as varying inflow angles as a function of the fans’ throttling state or operation point, respectively. Consequently, even at highly turbulent inflow conditions, the leading edge broadband noise not necessarily needs to represent the dominant noise source since it can be masked by the aforementioned additional effects of tonal and/or broadband character. Hence, when implementing leading edge serrations in rotating systems, the developer needs to deal with various effects, not yet considered for the single aerofoil investigations. To describe the transferability of serrated leading edges, the current study focuses on directly comparing the aeroacoustic effect of leading edge serrations for the single aerofoils and rotating machinery through low-pressure axial fans. The basic idea of the present study is to analyze the aeroacoustic noise reduction potential of single stationary NACA 65(12)-10 aerofoils, which are also commonly used for rotating applications. In a second step, the identical aerofoil type, including the leading edge serrations, is scaled and employed for the design of low-pressure axial fans, enabling a direct comparison between the two considered systems.

As it is indicated by the grey hatching in Figure 1, the radiated noise increases significantly at inflow conditions of elevated turbulence. In reverse conclusion, this low-to-mid-frequency region characterizes the maximum noise reduction potential when implementing e.g., serrated leading edges or any other device affecting the radiation of turbulence-ingested leading edge noise.

Figure 1 serves to emphasize the increased complexity of the acoustic pattern when comparing a full rotor to an isolated stationary aerofoil at comparable operation conditions, which include (a) comparable inflow angles, (b) an identical aerofoil/blade geometry, and (c) comparable inflow conditions using $U_0$ and the turbulence intensity $Tu$. 

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Speaking of broadband noise reduction due to leading edge serrations, the spectral sound power level reduction $\Delta PWL$ (Equation (6)) is obtained by subtracting the acoustic signature of a serrated aerofoil $PWL_{Serr}$ from that of an aerofoil with a straight leading edge $PWL_{BSLN}$. For isolated stationary aerofoils, the resulting spectral noise reduction is known to continuously increase from low to high frequencies [6,17], where the maximum is reached at the point of intersection, at which aerofoil self-noise due to the turbulent boundary layer starts to become increasingly dominant, forcing a decreasing performance for frequencies beyond this point. On this basis, a recent study by Chaitanya et al. [6], extending initial studies by Kim et al. [7], provides a rudimentary scaling law by which the spectral noise reduction $\Delta PWL$ is stated to follow Equation (1), with the prefactor generally being $a_s = 10$. The upper limit of the possible noise reduction can be achieved with $b_s = 10$ at an optimum ratio of serration wavelength and transversal turbulence length scale $\lambda/\Lambda_t \geq 4$ and takes place in the low-to-intermediate frequency range in the form of the amplitude-based Strouhal number $Sr_A$. Note that even though both constants $a_s$ and $b_s$ define the maximum noise reduction capability, the prefactor $a_s$ controls the slope of the trends, whereas $b_s$ controls the parallel shift of the noise reduction:

$$\Delta PWL = PWL_{BSLN} - PWL_{Serr} = a_s \cdot \lg(Sr_A) + b_s \quad \text{with} \quad Sr_A = \frac{f \cdot A}{U_0}. \quad (1)$$

Continuatively, the current study aims at answering the question if and how these aeroacoustic scaling laws also apply in the rotating context. This is of importance since it assists in assigning the causative mechanisms of the noise reduction for the tested rotors to the known mechanisms at isolated aerofoils. In a more general context, this analysis is expected to provide valuable information in assessing if the already known effects assigned to leading edge serrations still play the key role in reducing rotor noise or if there are effects that are more prominent.

Prior extracting the spectral scaling in the rotating domain, a valid data basis for isolated aerofoils of the identical geometric design was generated by Biedermann et al. [18], who performed aeroacoustic (and aerodynamic) characterization of the chosen NACA 65(12)-10 aerofoils via an extensive aeroacoustic beamforming study. The main advantage of this specific setup, however, is the possibility to exclude all the unwanted and distracting noise sources stemming from the aerofoil trailing edge, the open jet, the turbulence grids installed or even from the turbulent boundary layer. More recently, a similar approach was also followed by Bampanis et al. [19] for flat plate aerofoils, differentiating between the spectral contributions of leading edge noise and trailing edge noise.

For the current study, testing serrated aerofoils of varying serration amplitude $A$ and serration wavelength $\lambda$ by comparing the spectral noise composition to a straight leading edge baseline aerofoil, results in the spectral noise reduction pattern $\Delta PWL$ shown in Figure 2. Generally, the proposed spectral scaling law can be confirmed, even though higher prefactors of $a_s = 15$ according to Equation (1) are obtained, which can be attributed to the absence of aerofoil self-noise, usually attenuating the maximum noise reduction in the mid-frequency $Sr_A$-range. The upper limits of noise reduction are obtained at maximum amplitudes ($b_s = 8.5$) and minimum wavelengths ($b_s = 10$) [18]. Most interestingly, the optimum $\lambda/\Lambda_t$-ratio defined by Chaitanya et al. [3,6] is $\lambda/\Lambda_t \approx 2$ for maximum decorrelation effects and $\lambda/\Lambda_t \approx 4$ for maximum interference effects, enclosing the observed optimum of $\lambda/\Lambda_t = 2.6$ in Figure 2.
which, in reverse conclusion, allows analyzing and identifying the net-noise-reduction potential of the rotor is designed according to the isolated aerofoil approach [21], where the NACA 65(12)-10 present as well as of previous studies is to provide a low-speed axial fan of minimum complexity, and aeroacoustic performance of low-pressure axial fans with and without leading edge serrations. The standard [20] was developed which allows for simultaneous characterization of the aerodynamic and acoustic performance independent of the tested rotor design. Excessive preliminary measurements via hot wire anemometry [22] to remain independent of the tested rotor design. Excessive preliminary measurements via hot wire anemometry [22] results in the spatial velocity

\[ Tu \leq 0.35 \text{ m}, \text{ chord} = 0.15 \text{ m}. \] Figure adopted from [18].

2. Materials and Methods

To make first steps towards rotating applications, a test rig (Figure 3a) according to the ISO 5136 standard [20] was developed which allows for simultaneous characterization of the aerodynamic and aeroacoustic performance of low-pressure axial fans with and without leading edge serrations. The rotor is designed according to the isolated aerofoil approach [21], where the NACA 65(12)-10 fan blades are twisted in the spanwise direction to meet optimum incidence for all circumferential sections at design conditions. The test rig, as well as the data acquisition procedure, is identical to previous studies by the authors and is described more detailed in [22,23]. However, the focus of the present as well as of previous studies is to provide a low-speed axial fan of minimum complexity, which, in reverse conclusion, allows analyzing and identifying the net-noise-reduction potential of serrated blades in the rotating frame. Therefore, complex blade geometries such as blade skew and blade dihedral are intentionally avoided.

Implementing coarse biplane square grids [24] upstream of the rotor allows to vary the level of the incoming turbulence in a range of 2.6% \( \leq Tu \leq 12.1\% \) for the rotor plane, where the mean longitudinal velocity \( U_0 \) serves as the denominator of the turbulence intensity \( Tu \) to remain independent of the tested rotor design. Excessive preliminary measurements via hot wire anemometry were carried out by employing a rotating duct and the hot wire anemometry [22], resulting in the spatial velocity
distribution for the rotor plane as can be seen from Figure 4. Circumferential averaging of the data obtained leads to more general profiles of the incoming $T_u$, the longitudinal velocity as well as the transversal integral length scale $\Lambda_T$ (Figure 4b), making apparent the strong influence of the duct boundary layer on the resulting profiles. Representative single number values are obtained by averaging over a radius of $R_{Duct} = 0.15$ m to neglect influences of the wall boundary layer (Figure 4a). Preliminary studies on the power spectral density of the turbulent energy [23] showed it to scale-well with the turbulent cascade theory [25], resulting in scaling with $f^{-5/3}$ in the inertial range and with $f^{-7}$ in the dissipation range. Deviations from the model are, once again, observed close to the duct wall, though generally proving the turbulence conditions being of near-isotropic nature.

![Figure 4](image_url)

**Figure 4.** (a) Local distribution of longitudinal velocity; (b) Circumferentially averaged turbulent properties vs. the radial duct position for the tested turbulence grids at $n = 2000$ min$^{-1}$, $T_u = 12.1\%$, and measurement plane = rotor plane.

For the design of the serrated leading edges, the maximum chord $C$ of the blades was kept constant, resulting in different amplitude-dependent wetted surfaces of the fan blades as can be seen in Figure 5. An alternative approach would be to keep the mean chord constant, resulting in an extension of the local blade chord by $A/2$. The choice for the former design approach mainly serves three reasons:

1. A constant maximum blade chord results in only one baseline reference case for comparison as well as in a constant blade thickness for different serration geometries.
2. Keeping constant maximum solidity $\sigma_S$ prevents amplitude-dependent interaction effects of successive blades at solidities $\sigma_S \geq 0.7$.
3. Pursuing a conservative approach that remains close to practical applications, in which serrations might be included as a substituting technology at limited installation space by simply replacing previously mounted straight blades.

The aerodynamic performance is described via the non-dimensional flow coefficient $\varphi$ in Equation (2) and the pressure coefficient $\psi$ (Equation (3)) at iso-speed $n = 2000$ min$^{-1}$. Note that due to the specific setup and the location of the pressure sensors, the pressure coefficient $\psi$ is defined by the static pressure rise $\Delta P$ and the grid-dependent pressure loss $\Delta P_{Grid}$ (compare Figure 3a). The efficiency of the fan assembly $\eta_{System}$ in Equation (4) eventually serves to describe the relation of electric demand $P_e$ vs. the aerodynamic output $P_{aero}$. The small amplitude-dependent differences in the blade surface area (see Figure 5) naturally affect the aerodynamic performance in terms of static pressure rise $\Delta P$ as well as the flow rate $Q$. For comparison purposes, these differences require compensation. In contrast to the coefficients of lift and drag, for which a normalization by the wetted surface takes place for single aerofoils, the flow and pressure coefficients of rotating machines offer no
such compensation mechanisms. Therefore, preliminary measurements for straight blades of a varying chord are carried out by testing three different rotors with straight leading edges [23]. The surface of the three sets of rotor blades equals the wetted surface of the serrated blades with maximum (C/C₀ = 0.83), intermediate (C/C₀ = 0.91), and no (C/C₀ = 1) serration amplitude. Testing these scaled baseline blades, instead of the serrated blades, prevents including possible flow-dependent effects of leading edge serrations, which might affect the flow rate or the pressure rise.

![Figure 5](image)

**Figure 5.** Schematic of leading edge design including measures of importance. Both blades exhibit equal NACA 65(12)-10 properties. (a) Baseline case with a straight leading edge; (b) Serrated design, where grey hatching indicates reduced wetted area of the blade.

The results shown in Figure 6 indicate the (wetted) surface of the blades to contribute linearly to the static pressure rise Δp. The individual share of each semi-infinite radial element, however, scales with the circumferential velocity \( U_{rot} \) (Equations (2) and (3), where the required rotor diameter is defined by the hub diameter \( D_{Hub} \) plus the (representative) blade span \( S \)). Consequently, the circumferential velocity \( U_{rot} \) of the pressure coefficient \( \psi \) (Equation (3)) is defined according to an area-equivalent blade span \( S_{Rep} \) (Equation (3) and Figure 5), which is a function of the removed serration area \( A_{Serr} \) (Equation (5)) from the initial blade area \( A_{Blade} \):

\[
\psi = \frac{\Delta p / \rho}{\frac{U_{rot}^2}{2}} = \frac{\pi \cdot n \cdot (D_{Hub} + 2 \cdot S_{Rep})}{S \cdot C - A_{Serr}},
\]

\[
\eta_{system} = \frac{P_{aero}}{P_{el}} = \frac{\Delta p \cdot \dot{Q}}{U_{rot} \cdot A_{el}},
\]

\[
A_{Serr} = \frac{2S}{A} \int_{0}^{\pi} A \cdot \sin(2\pi / \lambda \cdot x) \, dx.
\]

In terms of acoustics, a microphone arrays at the discharge side of the fan unit enables gathering reliable and stable data, non-affected by the grid self-noise on the suction side. This array consists of three one-quarter inch wall-mounted condenser microphones, distributed circumferentially at the duct wall. Note that no beamforming is applied to the rotating application but that the spectral average of the microphone signals is used for further processing towards the local sound pressure level SPL (Equation (6)) with \( p_{RMS} \) being the effective sound pressure of the gathered signals and \( p_0 \) the reference value by means of the human threshold of audibility at 1 kHz. Continuatively, the overall sound pressure level OASPL is defined according to Equation (7) in the given frequency band 10 Hz ≤ f ≤ 10 kHz. Eventually, normalization by the enveloping surface of the noise sources \( A_E \)
as well as compensating for varying ambient conditions in terms of fluid density $\rho$ and speed of sound $c$, allows defining the local sound power level $PWL$ (Equation (6)). This is followed by the overall sound power level $OAPWL$ (Equation (7)). Note that for a ducted fan, the duct radius $R_{Duct}$ limits the enveloping acoustic surface $A_E$. Concerning the previously discussed compensation of the amplitude-dependent blade surface, also the sound power levels of the fan are monitored in Figure 6. Unlike for the aerodynamic properties, highly similar results are obtained for the $OAPWL$, indicating the wetted surface of the blades being only of secondary importance for the aeroacoustic signature. This is meaningful insofar as the level-dominant noise sources of the blades are the blade-tip region, the trailing edges, and the leading edges. Since the radial extension of the blades does not change with or without applying serrations or while varying the blade chord, also no differences in the noise radiation are obtained [2, 23]:

$$PWL = SPL + \left[ 10 \log \left( \frac{A_E}{A_0} \right) - 10 \log \left( \frac{\rho c}{\rho_0 c_0} \right) \right], \quad SPL = 10 \log \left( \frac{p_{RMS}^2}{P_0} \right)$$

(6)

$$OAPWL = OASPL + \left[ 10 \log \left( \frac{A_E}{A_0} \right) - 10 \log \left( \frac{\rho c}{\rho_0 c_0} \right) \right], \quad OASPL = 10 \log \left( \sum_{i=0}^{i=f_{max}} \frac{p_i^2}{p_0^2} \right)$$

(7)

![Figure 6. Validation of scaling approach by varying the chord length C of the baseline blades with $C_0 = 75$ mm. (a) Non-dimensional static pressure rise $\psi$; (b) Aerodynamic efficiency $\eta$; (c) Overall sound power level $OAPWL$ (Equation (7)).](image)

To gain deeper insights into the noise reduction mechanisms, resolving the spectral pattern of the data is required. Based on preliminary analysis of the signals [16], partitioning of the spectral content into its broadband and its discrete components proved to be meaningful since the underlying noise generation mechanisms are of different physical origin [26]. To split the rotor-speed-dependent components from those of broadband character, a customized one-dimensional median filter of the 30th order is applied to the original signal. In doing so, a frequency band of ±7.5 Hz around the rotor’s fundamental speed, or an integer multiple thereof, is replaced by its median, thus neglecting peaks with high slopes, which, in this case, are representing the tonal components. This procedure results in a broadband signal without loss of spectral energy (Figure 7a). The tonal filter is specified vice versa, solely showing the chopped-off peaks of the signal. Adding up the tonal and the broadband level yields exactly the original signal.
3. Results

3.1. Low-Pressure Axial Fans: Aerodynamic Performance

Figure 8 shows the overall performance of the tested rotors in terms of aerodynamics at (a) varying serration wavelength and (b) serration amplitude. For brevity, the fan characteristic curves of the serration configurations tested as well as the baseline case are presented only at low turbulence intensity. Even though the full characteristic curves are analyzed, the fan design point can be stated to be at maximum efficiency, corresponding to $\phi = 0.20$. In terms of aerodynamics, the results obtained are highly comparable to those of previously investigated single aerofoils [23], showing maximum performance for small serration amplitudes and high wavelengths. Serrations with low wavelengths and high amplitudes tend to show poorer performance, which can be attributed to the continuous increase in drag due to the vortex-generating and crossflow effects of the serrations.

Figure 7. (a) Example of a sound power level spectrum for the baseline rotor with applied filters, separating tonal and broadband effects; (b) Boundary conditions of customized filters [16].

Figure 8. Characteristic curves of pressure vs. flow coefficient for different rotor configurations. (a) Varying serration wavelength; (b) Varying serration amplitude.
3.2. Low-Pressure Axial Fans: Spectral Broadband Noise Reduction

To compare the broadband noise reduction between single aerofoils and the rotating application, the gathered signals are filtered in the frequency domain according to Section 2 and only the resulting broadband spectra are further processed towards the spectral noise reduction as was done for Figure 2. Once again, the frequency is normalized via the Strouhal number (Equation (1)), based on the serration amplitude. To comply with the definition of the $Tu_0$, for the Strouhal number, the longitudinal velocity at the rotor plane $U_0$ is chosen instead of taking the circumferential rotor mid-span velocity $U_{rot}$.

Figures 9 and 10 show the spectral noise reduction at varying turbulence intensities for the serrated rotors tested. According to the scaling of the spectral noise reduction discussed in Section 1, the results of the post-processed broadband signals are fitted via the least-squares minimization approach to the scaling laws by adapting the slope-determining prefactor $a_s$. This is followed by defining a common offset factor $b_s$, controlling the parallel shift. Note that the $b_s$ is matched only at optimum design conditions of the serrations. The obtained trends reveal a quite similar logarithmic scaling as for single aerofoils, where maximum serration amplitudes and small serration wavelengths show the highest potential for reducing rotor-turbulence interaction noise. Modulating the incoming turbulence reveals the noise reduction capability to be scaling with the slope-determining prefactor $a_s$, which extends the currently known trends for isolated stationary aerofoils since, in direct comparison, turbulence of significantly higher levels is generated for the rotating application. The prefactors show to continuously increase from $a_s = 10$ for the lowest $Tu = 2.6\%$ (Figure 9a) to $a_s = 22$ for the highest $Tu = 12.1\%$ (Figure 10c), leading to local reductions of the sound power level of up to $\Delta PWL = 14\,\text{dB}$. In conclusion, the common spectral logarithmic scaling (Equation (1)) for both isolated aerofoils and full rotors, indicates a reduction of leading edge broadband noise following the well-known aeroacoustic noise reduction mechanisms of serrated leading edges (compare Section 1). At least for the broadband noise, this enables a direct transfer from stationary aerofoils to rotating applications for operation conditions close to the design point $\phi \approx 0.18$.

The obtained scaling laws for the broadband noise reduction hint at relatively high prefactors $a_s$ when compared to the existing literature. However, the differences to previous studies can be attributed to the fact that, first, previous studies are focusing on rigidly mounted single aerofoils in turbulent streams. For these setups, it is not possible to generate conditions of homogeneous turbulence of $Tu > 6\%$ using passive turbulence generators as e.g., coarse grids. Consequently, the isolated stationary aerofoils are tested at moderately low turbulence intensities, which might be an argument for the lower prefactor $a_s$. In reverse conclusion, testing at similar $Tu$ level for both isolated aerofoil and the full rotor is expected to lead to a comparable spectral scaling. Second, the high prefactors $a_s$ for the rotating

![Figure 9](image-url)
applications result from substantially higher $Tu$-Levels investigated, when compared to the isolated aerofoils. The initial spectral scaling law was defined by Chaitanya et al. [6] who did not investigate effects on the prefactor $a_s$ since in their study the $Tu$ and thus the integral length scales were not varied in wide margins. Varying the serration wavelength and the amplitude mainly showed effects on the parallel shift of the noise reduction, as it can be described by the constant $b_s$. Accordingly, for the presented study a constant prefactor $a_s$ can be defined for each turbulent case where the second constant $b_s$ is controlled by the optimum serration amplitude $A$ and an optimum ratio of serration wavelength and integral length scale $\lambda/\Lambda_T$.

At off-design conditions, however, the broadband leading edge noise not necessarily represents the dominant acoustic source. With reducing flow coefficients, rotor-specific acoustic effects such as separation noise and reverse flow effects from the tip-gap region as well as rotor speed-dependent tonal effects increase in relevance. Consequently, these effects also affect and attenuate the overall noise reduction potential of serrated rotors. This is evidenced in Figure 11, which shows the comparison of the spectral noise reduction capability at different on-design and off-design conditions at iso-speed of the rotor. At flow coefficients $\phi > 0.18$, the grid-generated broadband noise is efficiently reduced, whereas at partial loading of the fan at $\phi \approx 0.17$ significantly stronger low-frequency components are induced and reduced.

![Figure 10](image1.png)

**Figure 10.** Spectral sound power level reduction $\Delta$PWL of the tested rotors at maximum flow coefficient $\phi$ and varying $Tu$. 20th-order median-filtered signals of broadband components only. Additional indication of the $\lambda/\Lambda_T$-ratio. (a) $Tu = 7.5\%$; (b) $Tu = 9.6\%$; (c) $Tu = 12.1\%$.

![Figure 11](image2.png)

**Figure 11.** Spectral sound power level reduction $\Delta$PWL at varying flow coefficient for two rotor designs (a) A22A13; (b) A14A4.
Minimum flow coefficients again show a log-dependent scaling of the noise reduction, albeit at a considerably lower level. This void in the validity of the spectral scaling laws for flow coefficients $\varphi \leq 0.18$ serves as a strong indicator that the mechanisms of the noise reduction differ from the hitherto known effects of leading edge serrations. More specifically, for the aerodynamic instability region of the fan characteristic curves, distinct aerodynamic effects such as a serration-induced delay in the onset of stall are considered being the key-effects in obtaining the significant overall noise reduction shown in Figure 12. The known aeroacoustic effects of decorrelation and interference are only of secondary importance for $\varphi \leq 0.18$.

![Figure 11. Spectral sound power level reduction $\Delta P_{WL}$ at varying flow coefficient for two rotor designs (a) A22$\lambda_{13}$; (b) A14$\lambda_{4}$.

![Figure 12. OAPWL of rotor equipped with leading edge serrations of varying serration amplitude, serration wavelength $\lambda$, and incoming $Tu$. Grey hatching indicates the aerodynamic optimum range of operation. (a) Varying amplitude at $Tu = 2.6\%$; (b) Varying amplitude at $Tu = 12.1\%$; (c) Varying wavelength at $Tu = 2.6\%$; (d) Varying wavelength at $Tu = 12.1\%$.

3.3. Low-Pressure Axial Fans: Overall Acoustic Performance

To assess the applicability of the spectral scaling laws for leading edge serrations requires a more general analysis of the aeroacoustic noise reduction pattern of the investigated low-pressure axial fans. In terms of acoustics, the overall effect of the tested rotors with and without leading edge serrations in Figure 12 shows that the baseline rotor radiates higher noise at all operation points. For maximum flow coefficients, the overall noise reduction is $\Delta OAPWL \leq 2.5$ dB. The most distinct differences to the baseline rotor, however, occur in the transition region from pre-stall ($\varphi \geq 0.18$) towards instability ($0.13 \leq \varphi \leq 0.18$) leading to an increase of the noise reduction potential up to $\Delta OAPWL \leq 6$ dB for the high turbulent case (Figure 12b). Here, the serrations are supposed to shift the onset of the (aeroacoustic)
stall towards smaller flow coefficients when compared to the baseline rotor. Given the fact that this shift is less distinct for the aerodynamic performance (Figure 8) leads to the hypothesis that small-scale separation at single blades is suppressed, not-yet affecting the overall pressure rise of the full fan.

The underlying effect is suspected to be an efficient reduction in small-scale separation due to the leading edge contour. This takes place via the vortex-generating character of the leading edge serrations [27,28], resulting in increased stability of the blades’ boundary layer as well as in an efficient shift of coherent structures in the blade tip region towards lower flow coefficients, as described in previous studies of the authors [16]. The known decorrelation and interference effects of the leading edge serrations [3] are still present though play a minor role in terms of the overall noise reduction. In consequence, for the instability region, the overall noise reduction results from a combination of aerodynamic and aeroacoustic effects of the leading edge serrations. The observed aeroacoustic shift tends to be more distinct at high turbulence, clearly scaling with the serration amplitude (Figure 12b). For the low turbulent case (Figure 12a,c), the shift benefits from the maximum noise reduction potential at maximum serration amplitudes, though generally showing a reduced extend. However, the resulting acoustic differences to the baseline case exceed those at high turbulence, resulting in an improved noise reduction potential (Figure 12b,d). This is meaningful insofar as the aerodynamic onset of the stall is more distinct for the high turbulent case compared to the already high OAPWL at pre-stall and high incoming turbulence. The effect of the serration wavelength $\lambda$, illustrated in Figure 12c,d, is of reduced impact when compared to the serration amplitude. Small wavelengths lead to a slight attenuation of the radiated noise which is particularly true for the pre-stall region at high flow coefficients. Generally, the reduced effect of the serration wavelength is in close agreement with recent literature for isolated aerofoils [3,4,17].

3.4. Low-Pressure Axial Fans: Broadband vs. Total Noise Reduction

Based on the overall sound power level in Figure 12, it is difficult and intricate to conclude on the broadband leading edge noise reduction potential of serrated rotors as well as the underlying physical mechanisms, in particular, once again highlighting the need to take into account the spectral composition of the noise reduction. In this context, the spectral composition of the noise reduction is extracted separately for the broadband components and the total noise signature. The results are presented in Figures 13 and 14, showing the contrasting juxtaposition for three different operating points within the optimum range of operation (compare Figure 12). At flow coefficients $\varphi \geq 0.18$, assigned to the pre stall region (Figure 13), where no relevant separation takes place, the spectral noise reduction for both broadband noise as well as total noise can be derived using the previously defined scaling functions. This hints at the dominance of the aeroacoustic working principles of leading edge serrations in this region. Analysis of the slope-determining prefactor $a_s$ as well as the offset $b_s$ results in a clear devaluing when comparing broadband and total noise reduction. The reduction of low-frequency broadband noise (Figure 13a,c) is equalized by rotor noise of discrete character, resulting in only little total noise reduction for the low-frequency region (Figure 13b,d). Moreover, the presence of blade tip effects, scaling with the rotational speed further attenuate the noise reduction for the mid-frequency region. The resulting total noise reduction still is of significant order even though the initially defined reduction potential shows to be affected by additional rotor effects of both aerodynamic and acoustic nature. In terms of serration parameters, highly similar trends are observed for the broadband as well as the total noise reduction, enabling general statements of beneficial parameter combinations for maximum noise reduction.
trends are observed for the broadband as well as the total noise reduction, enabling general statements of beneficial parameter combinations for maximum noise reduction.

![Graphs showing broadband and total noise reduction](image)

**Figure 13.** Juxtaposition of spectral noise reduction $\Delta \text{PWL}$ for broadband and total noise while varying the serration parameters as well as the point of operation. (a) Broadband reduction at $\varphi = 0.233\%$; (b) Total reduction at $\varphi = 0.233\%$; (c) Broadband reduction at $\varphi = 0.203\%$; (d) Total reduction at $\varphi = 0.203\%$.

Entering the instability region at $\varphi = 0.17$ (Figure 14) shows a deviating pattern, making the hitherto known scaling laws obsolete. A significant increase in low-frequency noise reduction is observed for the broadband noise but also being present for the total noise reduction. This supports the initial statement of predominantly aerodynamic effects being present for the increase of the acoustic stall margin. These effects in the form of a prevented flow separation mainly take place in the low-frequency range, resulting in high absolute noise reduction.
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