High-Temperature Alkali Vapor Cells with Anti-Relaxation Surface Coatings

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Anti-relaxation surface coatings allow long spin relaxation times in alkali-metal cells without buffer gas, enabling free motion of the alkali atoms and giving larger signals due to narrower optical linewidths. Effective coatings were previously unavailable for operation at temperatures above 80°C. We demonstrate that octadecyltrichlorosilane (OTS) can allow potassium or rubidium atoms to experience hundreds of collisions with the cell surface before depolarizing, and that an OTS coating remains effective up to about 170°C for both potassium and rubidium. We consider the experimental concerns of operating without buffer gas at high vapor density, studying the stricter need for effective quenching of excited atoms and deriving the optical rotation signal shape for atoms with resolved hyperfine structure in the spin-temperature regime. As an example of a high-temperature application of anti-relaxation coated alkali vapor cells, we operate a spin-exchange relaxation-free (SERF) atomic magnetometer with sensitivity of 6 fT/√Hz and magnetic linewidth as narrow as 2 Hz.

I. INTRODUCTION

Polarized alkali atoms lose their spin coherence after colliding with the walls of a glass vapor cell, limiting their spin-polarization lifetime and necessitating the use of either an anti-relaxation surface coating or a buffer gas in order to suppress the effects of wall relaxation. Paraffin is the most effective known coating, allowing alkali atoms to bounce up to 10,000 times off the cell wall without depolarizing [1], and it is used in applications including magnetometry [2], frequency reference [3], spin squeezing [4], slow light [5], and quantum memory [6]. In particular, modern alkali-metal magnetometers offer comparable or superior sensitivity to other magnetic field detectors, leading to recent interest in the study of the anti-relaxation properties of paraffin and other materials [7, 8, 9, 10, 11]. Much of this effort has focused on finding another coating as effective as paraffin but with better high-temperature stability, since paraffin melts and is ineffective above roughly 80°C. The most sensitive atomic magnetometers operate at higher temperatures than this in order to achieve large vapor density (typically \(10^{12-10^{14}} \text{ cm}^{-3}\)), including spin-exchange relaxation-free (SERF) vector magnetometers for detection of very weak fields [12, 13], scalar magnetometers for precise measurement of the amplitude of fields [14], and radio-frequency magnetometers for detection of oscillating fields [12, 16]. Due to the unavailability of appropriate surface coatings, all previous implementations of these high-density alkali-metal magnetometers have instead used cells filled with buffer gas, which slows diffusion of polarized alkali atoms to the cell walls.

It was recently shown [17] that a coating of octadecyltrichlorosilane (OTS) can allow alkali-metal atoms to bounce off the cell wall up to 2,000 times without depolarizing, although the quality of the coating is highly variable and levels of several hundred bounces are more typical. The OTS molecule resembles paraffin, containing an 18-carbon alkane chain, except with a silicon head group that chemically binds to the glass surface, enabling an OTS film to survive intact at higher temperatures than a paraffin film. Here we demonstrate that a multi-layer OTS coating operates at temperatures up to about 170°C, at which point we observe aging of the coating. We present the first use of anti-relaxation coated cells for high-density atomic magnetometry by implementing a SERF magnetometer using OTS-coated vapor cells. We discuss the advantages of coated cells over cells with buffer gas for high-density magnetometry, as well as experimental concerns such as more stringent quenching gas pressure requirements, and we derive the optical rotation signal profile in the spin-temperature regime for atoms with resolved hyperfine structure.

II. ADVANTAGES OF COATED CELLS FOR MAGNETOMETRY AND PRACTICAL CONSIDERATIONS

Coated cells have several practical advantages over buffer gas cells that allow for easier realization of high magnetic field sensitivity. In the absence of polarization-destroying collisions with buffer gas atoms, the magnetic linewidth can be much narrower. Coatings are particularly advantageous for miniature cells, which otherwise require very high buffer gas pressure to prevent wall collisions, resulting in broad linewidths [18]. An anti-relaxation coating can be considered “sufficient” for a given alkali metal and cell size if it operates at high enough temperature that the spin-polarization lifetime is dominated by alkali-metal spin-destruction collisions at this temperature rather than wall collisions. For example, for a spherical cell with radius \(r_0\), the number of bounces required to satisfy this condition is \(N > 3/[4r_0\sigma_{sd}n(T)]\), where \(\sigma_{sd}\) is the alkali-metal spin destruction cross-section and \(n(T)\) is the density of alkali-

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metal atoms as a function of temperature. Once the vapor density is high enough to meet this condition, any improvement in the coating quality will not affect significantly the lifetime. Under these conditions the magnetometer can reach the fundamental sensitivity limit set by the spin-destruction cross-section of the alkali-metal atoms. Here for the first time we demonstrate a coating of sufficient quality for Rb atoms in a ~1 cm cell.

Individual alkali atoms are free to move about a coated cell, even with about 10-50 Torr of quenching gas to prevent radiation trapping. The entire cell may thus be used as the active measurement volume without needing to expand the pump beam to fill the cell, since the wall coating allows some degree of polarization to be maintained even in the parts of the cell not actively being pumped. The probe beam likewise does not need to be greatly expanded because a large number of atoms are likely to pass through it during a polarization lifetime. Higher coating efficiency permits the use of smaller pump and probe beams. Rapid diffusion of atoms through the cell also enables partial suppression of magnetic field gradient effects on the polarization lifetime through motional averaging.

In addition, the lack of pressure broadening due to buffer gas results in narrow optical resonance linewidths and thus strong interaction between the atoms and the pump and probe beams. The combined effect of Doppler broadening, which has a Gaussian profile with width (FWHM) $\Gamma_G$, and the pressure broadening due to the buffer/quenching gas, which has a Lorentzian profile with width $\Gamma_L$, is described by a Voigt profile, as discussed in the Appendix. If the hyperfine structure of the alkali atom is partially or fully resolved, as is generally the case for cells with minimal pressure broadening, then it is necessary to consider separately the transitions between individual energy levels of the ground and excited states.

Coated cells require significantly less laser power than buffer gas cells to achieve the same optical pumping rate. Wall coatings are therefore highly favorable for portable and miniaturized devices where power consumption must be minimized. The inset of Figure 1 shows the maximum absorption cross-sections of D1 light calculated from Equation A.1 as a function of $\Gamma_L$ for $^{133}$Cs and $^{39}$K atoms at 160°C ($\Gamma_G=0.9$ GHz for $^{39}$K and 0.4 GHz for $^{133}$Cs). For narrow optical linewidths such that the hyperfine structure of the atom is partially resolved, it is necessary to determine from Equation A.1 the frequency of light that gives the largest cross-section for a particular linewidth $\Gamma_L$. The pressure broadening of the D1 resonance for potassium is 13.2 GHz/amg due to helium and 21.0 GHz/amg due to nitrogen, while the broadening for cesium is 19.9 GHz/amg due to helium and 14.8 GHz/amg due to nitrogen (1 amg=1 atm at 0°C). The need for some small amount of nitrogen (about 10-50 Torr) for quenching in coated cells requires a minimum $\Gamma_L \lesssim 1$ GHz, whereas high-density magnetometers typically employ up to several amg of helium as a buffer gas.

One of the primary challenges in achieving high magnetometer sensitivity is overcoming probe beam noise. The optical rotation of an off-resonant, linearly polarized laser beam can be used to measure the spin projection $P_s$ of the alkali atoms, as shown in Equation A.1, and noise in the measurement of beam polarization can obscure the rotation signal. The narrower optical linewidths of coated cells result in larger optical rotations, allowing for easier detection of small alkali polarization signals amidst the background of probe beam noise. For example, at frequencies below about 100 Hz, convection of the air that the probe beam passes through causes motion of the beam. The resulting 1/f noise can impair magnetometer performance by more than an order of magnitude; methods to deal with this noise, including the use of evacuated beam paths and modulation of the magnetic field to shift the magnetometer signal to a higher frequency, complicate the operation of the magnetometer. Narrower optical lines of cells with little buffer gas also result in higher optical depth on resonance for a given cell length and alkali metal density. Hence they are more advantageous for quantum-non-demolition polarization measurements where the improvement in signal-to-noise ratio scales as the square root of the optical density on resonance.

A narrow optical linewidth also results in strong attenuation of the probe beam, so while very large optical rotations can be obtained by tuning the probe beam close to resonance, the resulting polarimeter signal, which is proportional to $\theta(\nu)e^{-\alpha(\nu)t}$, may become small. Here $n$ is the density of the alkali vapor, and $t$ is the path length of the probe beam through the cell. The optimal probe

![FIG. 1: Scaling of the maximum optical rotation signal $\theta(\nu)e^{-\alpha(\nu)t}$ of the probe beam, taken at optimal detuning from resonance, as a function of buffer gas pressure broadening (FWHM) $\Gamma_L$. The potassium and cesium curves are normalized separately, and $\Gamma_G$ is set to its value at 160°C. The inset shows the maximum photon absorption cross-section as a function of $\Gamma_L$.](image-url)
beam detuning that maximizes this signal depends on the parameters of the system, including the buffer/quenching gas pressure and alkali density; if the hyperfine structure is optically resolved, then the individual resonances must be considered as in Equation \( \Delta Q \). Figure 1 shows the scaling of the maximum polarimeter signal for \(^{133}\text{Cs}\) and \(^{39}\text{K}\) atoms as a function of \( \Gamma_L \), for the case of a cell at 160°C and atomic density 5x10\(^{12}\) cm\(^{-3}\) with length 5 cm and \( P = 0.5 \). The curves for the two isotopes are normalized separately and should not be directly compared. Coated cells show an increase in signal of up to an order of magnitude over cells with several angstroms of buffer gas.

There are however practical considerations that must be addressed when operating at high alkali vapor density using coated cells, due to the narrow optical linewidths. One of these considerations is that the vapor may be too optically thick to allow the pump beam to penetrate far into the cell. In this case, the wall coating must be sufficiently good and the atomic diffusion must be sufficiently fast that the atoms are able to sample the front of the cell and get pumped during each polarization lifetime. Otherwise, the average polarization throughout the cell can be increased by modulating the frequency of the pump beam, so that when off resonance the beam travels further into the cell. The modulation amplitude should be chosen such that even the off-resonant light maintains a non-zero instantaneous pumping rate, and the modulation rate should be fast compared to the relaxation rate of the atoms to achieve significant polarization in the back of the cell.

Another consideration is the appropriate amount of quenching gas to include in the cell because radiation trapping is more likely to limit the polarization in cells with a narrower optical linewidth. Buffer gas cells can generally contain more quenching gas than is strictly necessary, since high buffer gas pressure broadens the optical linewidth and limits the atomic polarization lifetime to a much greater degree than the relatively small quenching gas pressure. On the other hand, coated cells should not contain an excessive amount of quenching gas, so as not to unnecessarily slow atomic diffusion, broaden the optical resonances, or cause additional spin destruction.

The polarization \( P \) attainable at low quenching gas pressure can be understood qualitatively from a modified version of the model given in [24]:

\[
P = \frac{R_{\text{OP}}}{R_{\text{OP}} + R_{\text{SD}} + K(M - 1)Q R_{\text{OP}} (1 - P)},
\]

where \( R_{\text{OP}} \) is the optical pumping rate, \( R_{\text{SD}} \) is the spin-destruction rate (including collisions with the wall, other alkali atoms, and quenching gas molecules), and \( M \) is the number of times a photon is emitted before escaping the cell. \( K \sim 0.1 \) is the degree of depolarization caused by a reabsorbed photon, which is determined by the nuclear slowing-down factor, as well as a geometrical factor due to some fraction of remitted photons having the same polarization as the pumping photons. \( Q \) is the probability of an alkali atom in the excited state decaying to the ground state by spontaneous decay rather than quenching, given by

\[
Q = \frac{1}{1 + R_Q \tau} = \frac{1}{1 + p_Q / Q}.
\]

Here, \( R_Q \) is the rate of collisions with quenching gas molecules, \( \tau \) is the excited-state lifetime, \( p_Q \) is the quenching gas pressure, and \( Q \) is the characteristic pressure that gives \( Q = 0.5 \).

In Equation 1, the last term in the denominator is the spin-relaxation rate due to absorption of reemitted photons, which we modify from the form given in [24] to include a factor of \( (1 - P) \) because polarized atoms can not absorb pump photons. This modification is necessary to account for the large polarization achieved in some applications at high alkali density; for example, radio-frequency magnetometers operate with nearly 100% polarization at high density in order to suppress spin-exchange broadening. The modified expression for \( P \) also better fits the high-density data in [24] than the original model.

### III. EXPERIMENT AND OBSERVATIONS

To demonstrate the effectiveness of coated cells in high-density magnetometry, we implemented a SERF magnetometer similar to those described previously [12, 13]. Orthogonal pump and probe beams were generated by distributed feedback diode lasers that were easily tunable over a large frequency range by adjusting the temperature and/or current of the diode. The frequency of the pump beam was modulated as necessary to achieve optimal polarization throughout the cell. The double-walled hot air oven was surrounded by five layers of \( \mu \)-metal shields with a shielding factor of about 10\(^5\), and magnetic field coils were used to cancel any residual fields.

The procedure for coating Pyrex glass with OTS was adapted from [28, 29] and was described in detail in [9]. The coatings were not prepared in the moisture-free conditions necessary for formation of a monolayer, and the thickness of the films has been measured to be roughly twice the length of an OTS molecule, indicating the presence of multiple layers at the surface [4]. The coated potassium cells were comprised of 5 cm diameter spheres with 1 mm inner-diameter stems containing potassium metal in natural abundance; the opening of the stem into
the cell was made as small as practical since polarized
atoms are lost when they enter the stem.

In addition to the evacuated cells described in [17],
we also made several additional potassium cells with ei-
ther 5.0 or 12.6 Torr of nitrogen for quenching of excited
atoms. We measured the quality of the coating in a par-
ticular cell by first polarizing the alkali atoms and then
turning off the optical pumping and observing the sub-
sequent polarization lifetime $T_1$. In order to determine
the number of bounces $N$ allowed in a spherical cell of
radius $r_0$ containing quenching gas, we consider diffusion
with the boundary condition given by [30] for the coated
surface:

$$\frac{\partial}{\partial r} P = \frac{-\tau P}{2N(2 - 1/N)D}, \quad (3)$$

where $P$ is the polarization as a function of position and
time, $\tau$ is the thermal velocity of the alkali atoms, and
$D$ is the diffusion constant. The solution to the diffusion
equation for the fundamental diffusion mode is given by
the following system of equations, which may be solved
numerically:

$$k \cot(kr_0) = \frac{1}{r_0} - \frac{\tau}{2N(2 - 1/N)D}, \quad (4)$$

$$\frac{1}{T_1} = Dk^2 + R_{\text{col}}, \quad (5)$$

where $k$ is the radial diffusion wave number, and $R_{\text{col}}$
is the spin-destruction rate due only to alkali-alkali and
alkali-quenching gas collisions. A similar solution may
be obtained for arbitrary cell geometry. The new cells
exhibited relaxation times in the range of 30-45 ms, con-
sistent with 400-600 bounces, though none matched the
2,000 bounces allowed by one of the evacuated cells. We
also measured the polarization lifetimes in two OTS-
coated rubidium cells to both be consistent with 700-
900 bounces. Recent observations of both monolayer
and multilayer OTS suggest that the quality of the film
as an anti-relaxation coating in a particular cell may be
determined by the fractional coverage of defect sites on
the surface [10]. The estimated numbers of bounces are
only approximate due to the uncertainty in the values
of the diffusion constants of potassium and rubidium in
nitrogen; we use $D=0.25$ cm$^2$/s for potassium [31] and
$D=0.14$ cm$^2$/s for rubidium [32] (at 273 K). The OTS-
coated cells made in our lab for this study and for related
studies are listed in Table I.

We found that the OTS coating could withstand tem-
peratures below 160°C without permanent damage in
the presence of both potassium and rubidium vapor, al-
though cells operating at 170°C displayed slow degra-
dation of coating performance on a time scale of days.
We measured the alkali density to be less than expected
from the saturated vapor pressure and found that it var-
ied by as much as a factor of 2 from cell to cell, with
observed densities at 170°C up to $9 \times 10^{12}$ cm$^{-3}$ for potas-
sium and $9 \times 10^{13}$ cm$^{-3}$ for rubidium. The maximum op-
erating temperature is the same for both species despite
the difference in density by up to an order of magnitude,
suggesting that the coating is damaged by collisions be-
tween individual alkali atoms and the silane head groups
attached to the surface; some minimum thermal energy
may be required to break the chemical bond between the
OTS molecules and the glass. For comparison, a mono-
layer OTS coating remains undamaged up to 190°C in
the presence of rubidium [8], and it can survive tempera-
tures up to 400°C when not exposed to alkali vapor [33].

Figure 2 shows measurements of the polarization life-
time $T_1$ over the course of several days in a rubidium cell.
The temperature was increased from 100°C to 170°C at
t=0, and it was returned to 100°C after the final measure-
ment was taken on each day. When at lower temperature,
the stem was actively cooled in order to collect the alkali
metal; this was found to reverse temporary reductions
of the polarization lifetime due to alkali condensation on
the walls of the main cell body. At higher temperature
$T_1$ is dominated by spin-destruction collisions between
rubidium atoms and is thus highly sensitive to fluctua-
tions in the vapor density, but a permanent reduction in
the coating effectiveness after each day of operation
at 170°C is evident from comparing the data taken at
lower temperature. The polarization lifetime never re-
covered, even after leaving the cell at lower temperature
with its stem cooled for a period of several days. We
speculate that patches of bare glass are slowly exposed
as OTS molecules are removed from the surface, resulting
in gradual degradation of the coating. This is the first
time that a sufficient anti-relaxation coating has been
demonstrated with rubidium vapor in a cell of this size,
and it raises the possibility of a rubidium SERF magnet-
ometer with an OTS-coated cell reaching its fundamen-

\begin{figure}[h]
\centering
\includegraphics[width=\textwidth]{figure2.png}
\caption{(Color online) Measurements of the polarization life-
time $T_1$ taken in an OTS-coated rubidium cell (#13) with
10 Torr of nitrogen quenching gas, showing degradation of
the coating after extended operation at 170°C. Note that at
170°C the relaxation time is dominated by collisions between
rubidium atoms, indicating that the surface coating is suffi-
ciently effective.}
\end{figure}
TABLE I: List of OTS-coated cells produced for this study and for related studies. The polarization is given for maximum pump beam intensity at a vapor density of $5 \times 10^{12}$ cm$^{-3}$, and the polarization lifetime $T_1$ is given as the maximum value measured for each particular cell. The number of bounces allowed by the coating for cells with quenching gas is approximated using the diffusion model described in the text.

| Cell | Size and Shape       | Alkali | Gas         | Max. Polarization | Max. $T_1$ (ms) | Bounces (Approx.) |
|------|----------------------|--------|-------------|-------------------|-----------------|------------------|
| 1    | 0.90" Diameter Sphere| K      | 26.0 Torr N$_2$ | 23                | 500             |                  |
| 2    | 0.90" Diameter Sphere| K      | 26.0 Torr N$_2$ | 24                | 550             |                  |
| 4    | 1.90" Diameter Sphere| K      | None        | 1.6              | 20              |                  |
| 5    | 1.90" Diameter Sphere| K      | None        | 2%               | 33              | 500              |
| 6    | 1.95" Diameter Sphere| K      | None        | 61               | 900             |                  |
| 7    | 1.96" Diameter Sphere| K      | None        | 145              | 2100            |                  |
| 8    | 2.00" Diameter Sphere| K      | 5.0 Torr N$_2$ | 40               | 500             |                  |
| 9    | 2.00" Diameter Sphere| K      | 5.0 Torr N$_2$ | 33               | 400             |                  |
| 10   | 2.01" Diameter Sphere| K      | 5.0 Torr N$_2$ | 46               | 600             |                  |
| 11   | 2.00" Diameter Sphere| K      | 12.6 Torr N$_2$ | 45               | 45              | 450              |
| 12   | 2.2 cm $\times$ 2.2 cm $\times$ 3.5 cm | $^{87}$Rb | 5 Torr N$_2$ | 51              | 850             |                  |
| 13   | 2.5 cm $\times$ 2.5 cm $\times$ 4.5 cm | $^{87}$Rb | 10 Torr N$_2$ | 80%             | 59              | 700              |

The long relaxation time allowed by an OTS coating enables magnetic resonance linewidths comparable to those observed in low-temperature paraffin cells and in buffer gas cells in the SERF regime. Near zero field there is no well-defined quantization axis, and spin-exchange relaxation is eliminated, so $T_1 = T_2$. The magnetic linewidth $\Delta \nu$ is then given by the optical pumping and spin-destruction rates as

$$2\pi \times \Delta \nu = \frac{1}{T_2} = \frac{(R_{OP} + R_{SD})}{q},$$

where the linewidth is given as the halfwidth at half-maximum (HWHM), and $q$ is the polarization-dependent nuclear slowing-down factor (see [34]). Figure 3 shows a resonance signal with linewidth of 2.3 Hz obtained at 150°C using the evacuated potassium cell that allows 2,000 bounces (Cell #7), taken with $R_{OP} \ll R_{SD}$ so that the linewidth is dominated by the collisions with the OTS-coated surface. Although radiation trapping limited the alkali polarization in this cell to about 2% even with high pumping rate, similar performance should be possible in cells with sufficient quenching gas and comparable coating effectiveness.

Radiation trapping also limited the polarization in the cells with quenching gas. The pumping rate should be equal to the spin-destruction rate for optimal performance of a SERF magnetometer, giving 50% polarization, but under this condition the polarization in the potassium cells was observed to be only about 5-10% at a density of $n=5 \times 10^{12}$ cm$^{-3}$. In contrast, in a rubidium cell with 10 Torr of nitrogen at the same density, we observe the expected polarization. Even with such low polarization, large optical rotation signals were observed in the potassium cells. A dispersion curve with an amplitude of 1.6 radians is shown in Figure 4 exhibiting the characteristic turn-over of the polarimeter signal once the optical rotation angle reaches $\pi/4$. Such large rotations have not been seen previously in SERF magnetometers using buffer gas-filled cells.

Magnetometers often operate using a feedback loop to lock to the zero crossing of the resonant dispersion curve, so a useful figure-of-merit is the slope at this point. A SERF magnetometer with its pump beam in the $\hat{z}$ direction and its probe beam in the $\hat{x}$ direction is primarily
sensitive to the magnetic field component along \( \hat{y} \); if this field is sufficiently small that the polarization remains nearly along \( \hat{z} \), then the magnetometer signal \( \theta \) given by Equation A.6 is proportional to

\[
    P_x \approx P_0 \frac{\gamma_e B_y (R_{OP} + R_{SD})}{(R_{OP} + R_{SD})^2 + (\gamma e B_y)^2},
\]

where \( \gamma_e = g_s \mu_B / \hbar \) is the gyromagnetic ratio of the electron \([12]\). In a potassium cell with 12.6 Torr of nitrogen and pumping rate equal to the spin-destruction rate, giving 8% polarization and HWHM of 6.5 Hz at \( n=5 \times 10^{12} \text{ cm}^{-3} \), we measured a slope \( \partial \theta / \partial B_y \) of 57 rad/mG near the point of optimal probe beam detuning, in agreement with Equations 7 and A.6. Tuning the probe beam closer to the optical resonance, we achieved a slope of 135 rad/mG. For comparison, in a square cell with length 2.2 cm and 2.9 amg of helium buffer gas at the same density, 50% polarization, and HWHM of 4.6 Hz, we measured a slope of 15 rad/mG at the point of optimal detuning, close to the predicted 17 rad/mG. Even accounting for the longer optical path length, the slope was larger in the coated cell despite a broader magnetic linewidth and significantly smaller polarization. The advantage should be even greater in cells with additional nitrogen to attain higher polarization while still maintaining a narrow linewidth \( \Gamma_L \).

Shown in Figure 4 is a magnetic field noise spectrum taken in an OTS-coated potassium cell without buffer gas at 150°C. The magnetometer sensitivity is 6 fT/√Hz, possibly limited by the noise of the magnetic shielding. The optical noise of the probe beam was measured in the absence of pumping light, so that the vapor was unresponsive to ambient field noise.

FIG. 4: A dispersion curve with amplitude of 1.6 radians measured in a coated cell (#11); rotations larger than \( \pi/4 \) radians cause the polarimeter signal to turn over.

IV. CONCLUSION

In summary, we have found that a multilayer OTS coating preserves alkali polarization at temperatures up to 170°C for both potassium and rubidium vapor, despite an order of magnitude difference in vapor density at that temperature, motivating further investigation of the interaction between alkali atoms and the OTS surface. We have demonstrated the use of coated cells in high-density alkali-metal magnetometry, showing that such cells permit narrow magnetic resonance linewidths and feature larger optical rotation signals than buffer gas-filled cells under similar operating conditions. An OTS coating that allows several hundred bounces was found to be sufficient for rubidium cells with dimensions of several cm near the maximum operating temperature.

We have also studied some of the experimental concerns specific to high-density alkali vapor with minimal pressure broadening, including the stricter requirements for quenching that cause additional depolarization from radiation trapping; indeed, radiation trapping limited the polarization in the potassium cells used for this study, so cells with additional quenching gas should show an even larger improvement over cells with buffer gas. All measurements were made with a SERF magnetometer,
but the results are equally valid for radio-frequency and scalar magnetometers operating at high density. In the Appendix we derive the shape of the optical rotation signal for alkali atoms with resolved hyperfine lines in the spin-temperature regime, which is typically the case for atoms at high density without pressure broadening from buffer gas. Anti-relaxation coatings will be an essential tool as the sensitivity of high-density magnetometers drives toward the attotesla level, underscoring the importance of developing more effective and reliable high-temperature surface coatings.

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APPENDIX

In cells with no buffer gas and a limited amount of quenching gas, the pressure broadened linewidth $\Gamma_L$ is comparable to the Doppler broadened linewidth $\Gamma_G$. For light of frequency $\nu$, the optical resonance lineshape is then described by a Voigt profile,

$$V(\nu - \nu_0) = \frac{2\sqrt{\ln 2/\pi}}{\Gamma_G} w(2\sqrt{\ln 2}[(\nu - \nu_0) + i\Gamma_L/2]/\Gamma_G),$$  \hspace{1cm} (A.1)

$$w(x) = e^{-x^2}(1 - \text{erf}(-ix)),$$  \hspace{1cm} (A.2)

where $\Gamma_L$ and $\Gamma_G$ are both given as full-width at half maximum (FWHM), $\nu_0$ is the resonance frequency, and $w(x)$ is the complex error function. For light near the D1 transition of an atom with nuclear spin $I$, the ground- and excited-state hyperfine levels are $F_g = I \pm 1/2$ and $F_e = I \pm 1/2$, respectively, and the resonance frequency for the transition $F_g \rightarrow F_e$ is $\nu_{F_g,F_e}$. The weight of this transition for unpolarized atoms is

$$A_{F_g,F_e} = \frac{(2F_g+1)(2F_e+1)}{2I+1} \left\{ 1/2 \ 1 \ 1/2 \right\}^2, \hspace{1cm} (A.3)$$

where the curly brackets denote the 6-$j$ symbol. The coefficients $A_{F_g,F_e}$ are listed in Table [11]. The photon absorption cross-section $\sigma(\nu)$ is given by [35]

$$\sigma(\nu) = \pi r_e c f \sum_{F_g,F_e} A_{F_g,F_e} \text{Re}[\nu - \nu_{F_g,F_e}], \hspace{1cm} (A.4)$$

where $r_e$ is the classical electron radius, and $f = 1/3$ is the oscillator strength.

Similarly, the optical rotation angle $\theta(\nu)$ of a linearly polarized probe beam propagating in the $\hat{x}$-direction is determined by the difference in the absorption cross-sections of $\sigma^+$ and $\sigma^-$ light. For atoms in the spin-temperature distribution [36], the relative weight of the transition $F_g \rightarrow F_e$ is therefore

$$B_{F_g,F_e} \propto A_{F_g,F_e} \sum_{m_F} e^{\beta m_F} \left[ \begin{array}{ccc} F_e & 1 & F_g \\ m_F + 1 & -1 & -m_F \end{array} \right]^2$$

$$- \left[ \begin{array}{ccc} F_e & 1 & F_g \\ m_F - 1 & +1 & -m_F \end{array} \right]^2, \hspace{1cm} (A.5)$$

where the sum is over all Zeeman sublevels of the ground state $F_g$, and $\beta$ is $\ln[(1 + P)/(1 - P)]$ is the spin-temperature parameter. These coefficients are themselves functions of the alkali atomic polarization, and they are listed in Table III in normalized form such that $\sum_{F_g,F_e} B_{F_g,F_e} = 1$. The total rotation angle is then given by

$$\theta(\nu) = \frac{\pi}{2} |r_e c f n P_z \sum_{F_g,F_e} B_{F_g,F_e} \text{Im}[\nu - \nu_{F_g,F_e}]|, \hspace{1cm} (A.6)$$

where $l$ is the path length of the probe beam through the cell, $n$ is the density of alkali atoms, and $P_z = \vec{P} \cdot \hat{x}$ is the component of alkali polarization along the probe beam direction. Equations (A.4) and (A.6) may also be used to describe the case of large pressure broadening due to high pressures of buffer gas, though $V(\nu - \nu_0)$ becomes nearly Lorentzian when $\Gamma_L \gg \Gamma_G$.

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TABLE II: Relative strengths of the individual D1 transitions $F_g \rightarrow F_e$ for photon absorption and optical rotation in Equations A.4 and A.6.

| Transition        | $I = 3/2$     | $I = 5/2$     | $I = 7/2$     |
|-------------------|---------------|---------------|---------------|
| $I - \frac{1}{2} \rightarrow I - \frac{1}{2}$ | $1/16$ | $105^5$ | $18(1+10P^2+3P^4)$ | $5/16$ | $7(1+10P^2+3P^4)$ | $7/108$ | $7(1+10P^2+3P^4)$ |
| $I - \frac{1}{2} \rightarrow I + \frac{1}{2}$ | $5/16$ | $35/108$ | $18(1+10P^2+3P^4)$ | $21/108$ | $9(1+10P^2+3P^4)$ |
| $I + \frac{1}{2} \rightarrow I - \frac{1}{2}$ | $5/16$ | $35/108$ | $18(1+10P^2+3P^4)$ | $21/108$ | $9(1+10P^2+3P^4)$ |
| $I + \frac{1}{2} \rightarrow I + \frac{1}{2}$ | $5/16$ | $7/27$ | $18(1+10P^2+3P^4)$ | $15/64$ | $64(1+10P^2+3P^4)$ |

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