Lepton Flavor Violation in SUSY GUT Model with Non-universal Sfermion Masses

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Abstract

We analyze lepton flavor violating $\tau \rightarrow \mu \gamma$ and $\mu \rightarrow e \gamma$ processes in SUSY GUT model in which sfermions have special mass spectrum. It is assumed that only third generation sfermions which are contained in $10(Q, U_c, E_c)$ of SU(5) can have a different mass from the others. This mass spectrum is led from E$_6$ GUT model with horizontal symmetries. It is shown that branching ratios of $\tau \rightarrow \mu \gamma$ and $\mu \rightarrow e \gamma$ depend strongly on a right-handed stau mass. The weak scale stability requires the light stau, so large decay rates can be expected in this scenario. When the stau mass is around 150 GeV and $\tan \beta \sim 10$, the branching ratios can be larger than $Br(\tau \rightarrow \mu \gamma) \simeq 10^{-8}$ and $Br(\mu \rightarrow e \gamma) \simeq 5 \times 10^{-12}$, which are within reach of future experiments. In addition, this model has an interesting feature that the final state charged lepton tends to have the right-handed chirality.

1 Introduction

The measurement of the Lepton Flavor Violation (LFV) in charged lepton sector is one of the most important measurements to search for New Physics beyond the Standard Model (SM). Since the neutrino oscillations have been observed, the charged LFV processes can be expected to be non-vanishing. However, the SM with the Majorana neutrino masses leads too small LFV decay rates to be observed due to smallness of the neutrino masses. Thus, detections of the LFV processes means discovery of New Physics.

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In fact the supersymmetric extension of the SM leads generically large LFV decay rates, because of picking up the off-diagonal entries of slepton mass matrices (in substitution for neutrinos) in intermediate state. However, it is well known that Flavor Changing Neutral Current (FCNC) and CP violating processes are highly suppressed experimentally. They impose severe constraints on the minimal supersymmetric (SUSY) standard model (MSSM) parameter space\cite{2}. The simplest way to satisfy these FCNC constraints is to adopt the universal sfermion soft mass matrices at some scale.

In many analyses that have been done so far, the universal soft masses at the gravitational scale or at the grand unified scale have been assumed and the LFV decay rates are calculated by the non-universality which is induced by the radiative correction\cite{3,4}. For example, in the MSSM with the Majorana neutrino masses, the radiative correction induces the non-universal sfermion masses\cite{3}. Unfortunately, it is difficult to predict the LFV decay rates quantitatively in this scenario unless the Dirac neutrino Yukawa couplings are fixed, because such LFV decay rates strongly depend on the Dirac neutrino Yukawa couplings, which looks impossible to be measured directly. In SO(10) grand unified theory (GUT), the Dirac neutrino Yukawa couplings are related with the up-type quark Yukawa couplings. Then we can predict the LFV decay rates\cite{4}, but they are too large to be consistent with the experimental bound if the diagonalizing matrix of the fermions mass matrices for doublet lepton has the Maki-Nakagawa-Sakata\cite{5}(MNS)-like large mixings. In this direction, some special structure which suppresses the $\mu \rightarrow e\gamma$ process is required.

The assumption of universal soft masses is not necessarily required. For example, since the FCNC constraints for the first two generation fields are much more severe than for the third generation fields, the universal soft masses sometimes have been imposed only for the first two generation sfermion, which are realized if we impose non-Abelian horizontal symmetry, for example, U(2), under which the first two generation fields are doublets and the third generation fields are singlets\cite{6}. However, if the diagonalizing matrix of the fermions have the MNS-like large mixings, such sfermion mass spectrum leads to too large FCNC to be consistent with the experimental bound. Therefore, such non-universality must be introduced only for the sfermion whose fermionic superpartner has the diagonalizing matrix with the Cabibbo-Kobayashi-Maskawa\cite{7}(CKM)-like small mixings.

In the SU(5) SUSY-GUT, it is a reasonable assumption that the diagonalizing matrices of 10 representation fields have the CKM-like small mixings, while those of $\bar{5}$ fields have the MNS-like large mixings, because 10 representation includes the doublet quarks, and $\bar{5}$ includes the doublet leptons. Under this assumption, only the third generation sfermions of the 10 representation can have different masses from the others without contradicting with experimental constraints from various FCNC processes. In this paper, we study the LFV under the non-universal sfermion masses above.

Before examining the LFV, we summarize several characteristic features of the non-universal sfermion masses. First of all, the rotation matrix for 10 which makes fermions to mass eigenstate is expected to have the CKM-like small mixings, since 10 involves quark doublet. Therefore, large off-diagonal entries for 10 representation sfermion mass matrix do not arise after this rotation, even if the initial soft masses are not degenerate. Moreover, FCNC constraints among 1-3 or 2-3 generations are not so severe than that of 1-2 generations. Therefore, we can expect that non-degeneracy for third generation does not conflict the FCNC constraints. And it is important that we can expect larger FCNC for the third generation fields than in the usual universal sfermion mass case.
Second, the naturalness of the Higgs mass in MSSM requires that the gaugino masses, the higgsino mass, and the stop masses must be around the weak scale. In the above non-universality case, we can take the larger masses for the other sfermion masses than the third generation 10 representation without conflicting the naturalness arguments, because the both stops (left and right handed stops) are included in the third generation 10 representation of SU(5). In principle, we can take such mass larger than 1 TeV, which can weaken the various constraints from FCNC, electric dipole moments (EDM) and the muon $g - 2$, etc. related with the first two generation fields. Again, the FCNC related with the third generation fields can become relatively large, which may be detectable in future experiments. Finally, such non-universality of the sfermion masses is naturally realized in the E$_6$ SUSY-GUT model[8, 9] with SU(2) or SU(3) horizontal symmetry[10].

In this paper, we will analyze the lepton flavor violating $\tau \rightarrow \mu \gamma$ and $\mu \rightarrow e \gamma$ processes under this non-universal sfermion masses. The point is that the naturalness requires that the $10_3$ sfermion masses are $O(\Lambda_W)$, i.e., the right-handed stau mass becomes $O(\Lambda_W)$. We show that if mass of right-handed stau is near the weak scale, each LFV decay rate becomes sufficiently large to be found by near future experiments. Actually, the LFV decay rates are very sensitive to the right-handed stau mass. Thus, if $\tau \rightarrow \mu \gamma$ or $\mu \rightarrow e \gamma$ processes are discovered and the branching ratios are measured, this model may predict a mass of right-handed stau. We will see that this model has interesting feature, that is, this model indicates that the final state charged lepton tends to be right-handed, since main source of flavor violation comes from the Feynman diagram which includes the right-handed charged slepton.

This paper is organized as follows. In the next section, we will specify the model, and discuss how lepton flavor violating processes take place in this model. The results of our numerical study are given in Section 3. In Section 4, we will give a summary and discussion of our results.

2 Lepton Flavor Violation in this model

In this section, we discuss how lepton flavor violating decays take place in a SUSY-GUT model with the non-universal sfermion masses mentioned in the previous section. First, we assume that the SM gauge group SU(3)$_C \times$ SU(2)$_L \times$ U(1)$_Y$ is unified into SU(5). (Note that the following arguments can be applied to unified models with larger unified gauge groups, for instance, SO(10) or E$_6$.) Then, around the GUT scale, the Lagrangian for the SUSY breaking terms is given as

\[-\mathcal{L}_{\text{soft breaking}} = -\mathcal{L}_{\text{soft mass}} + (A_{ij}^u 10_i 10_j 5_H + A_{ij}^{d,e} 10_i \tilde{5}_j F_H
\]
\[+ A_{ij}^e 1 \tilde{5}_i 5_H + B \tilde{5}_H 5_H + \frac{1}{2} M_{1/2} \lambda^a \lambda^a + \text{h.c.}) , \tag{1} \]
\[-\mathcal{L}_{\text{soft mass}} = (m_{10}^2)_{ij} 10_i^\dagger 10_j + (m_{\tilde{5}_i}^2)_{ij} \tilde{5}_i^\dagger \tilde{5}_j + m_{\tilde{5}_i \tilde{5}_j}^2 \tilde{5}_i^\dagger \tilde{5}_j + m_{H_d}^2 5_H^\dagger 5_H + m_{H_u}^2 5_H^\dagger 5_H \tag{2} \]

where the tilded fields are regarded as sfermions, $\lambda^a$ is SU(5) gauginos, $10_i = (Q_i, \bar{U}_i, \bar{E}_i)$, $\tilde{5}_i = (\bar{D}_i, \bar{L}_i)$, $\bar{1}_i = \bar{N}_i$ ($i = 1, 2, 3$), $M_{1/2}$ is SU(5) gaugino mass, and $-\mathcal{L}_{\text{soft mass}}$ gives sfermions and Higgs soft mass terms. $5_H$ and $\tilde{5}_H$ include the down-type Higgs $H_d$ and the up-type Higgs $H_u$, respectively.

As mentioned in Introduction, we consider following forms for the sfermion mass
matrices.

\[
m_{10}^2 = \begin{pmatrix} m_0^2 & m_0^2 \\ m_0^2 & m_{30}^2 \end{pmatrix}, \quad m_{\tilde{5}}^2 = \begin{pmatrix} m_0^2 & m_0^2 \\ m_0^2 & m_{15}^2 \end{pmatrix}.
\]

The reasons are as follows:

- **Severe Constraints on the first two Generation:**
  There are severe constraints on the off-diagonal entries of low energy sfermion mass matrices from the various FCNC processes in the basis of the superfields in which all quark and lepton mass matrices are diagonal (super-CKM basis). This is famous as the SUSY-Flavor problem. In particular, the (1,2) component suffers from strong constraints by CP violating parameters of $K^0 - \bar{K}^0$ mixing, lepton flavor violating $\mu \to e\gamma$, and so on. Thus, we cannot release degeneracy between 1-2 generation, otherwise a large (1,2) element arises in super-CKM basis and it conflicts with experiments.

- **Large Neutrino Mixing and Constraints on 2-3 Generation:**
  It is known that there is a maximal mixing between 2-3 generation in lepton sector\([11]\). This large mixing sometimes is related with the mixing of $\tilde{5}$ since $\tilde{5}$ contains left-handed lepton doublet. Thus, if we release degeneracy between 2-3 generations in $\tilde{5}$, a large 2-3 component of $\tilde{5}$ is generated in super-CKM basis. It conflicts with constraints from $B^0 - \bar{B}^0$ mixing and $\tau \to \mu\gamma$. Therefore, we should assume degeneracy of 2-3 generation for $\tilde{5}$ soft masses. While, we can take a soft mass of the third generation of $\tilde{10}$ different from that of the other generation, since a mixing of $\tilde{10}$ is expected to be as small as CKM mixing.

- **Naturalness of the MSSM:**
  In the MSSM, there is no terrible fine tuning problem due to supersymmetric cancellation for quadratic divergence for radiative correction to Higgs mass square. Instead of the quadratic divergence, the radiative corrections are proportional to the SUSY breaking mass square, and therefore SUSY breaking mass scale must be around the weak scale $\Lambda_W$ to avoid some tuning if the couplings are $O(1)$. Among the various sfermion masses, only the stop masses must be the weak scale, while the other sfermion masses can be taken much larger than the weak scale because of the smallness of the Yukawa couplings. One of the advantages of the mass spectrum we assumed is that we can take all the sfermion masses much larger than the weak scale except the masses of sfermions which are contained in $10_3$. In such parameter region, several constraints in SUSY models, for example $g - 2$, EDM, FCNC, etc, are relaxed without loss of naturalness. Especially, A-term contribution to EDM or FCNC for the first two generations can be decoupled in this region. In the literature, it is argued that the stop masses are required to be larger than the weak scale to realize the Higgs mass larger than the lower bound $m_h > 114.4$ GeV obtained at LEP II. Such large stop masses lead to some tuning in the Higgs sector. This is called “the little hierarchy problem”\([12]\). However, as discussed in \([13]\), the stop masses around 300-400 GeV can be consistent with the LEP II experiments, if the lightest CP-even Higgs has a small $ZZh$ coupling. Therefore, some of the parameter region considered in this paper may lead to such small stop masses, but it is consistent with the LEP II results of the Higgs search experiment.
• \textbf{E}_6 \text{ GUT with } U(2) \text{ horizontal Symmetry:}

Introducing a non-Abelian horizontal symmetry is one of various interesting possibilities to realize the flavor blind nature of the sfermion masses\cite{6,14}. Most of the previous attempts adopt $U(2)$ or $SU(2) \times U(1)$ symmetry as the horizontal symmetry\cite{6}, which realize the universality of the first two generation sfermion masses and the large top Yukawa coupling, if we assign doublets for the first two generation fields and singlets for the third generation fields and the Higgs fields. Unfortunately, the universality of the first two generation fields is not sufficient to suppress the FCNC constraints especially when the diagonalizing matrix of fermion mass matrices have the MNS-like large mixings as we pointed out in the previous section. $E_6$ GUT $\times U(2)$ Horizontal Symmetry model\cite{10} succeeds to give not only the observing large hierarchy of fermion masses but also the sufficient universality of the sfermion masses to avoid FCNC or EDM constraints in a simple way even when the diagonalizing matrix has the MNS-like large mixings. It is essential that this model can naturally realize the sfermion mass spectrum which we discussed in this paper because of an $E_6$ nature.

The superpotential is given at the GUT scale as follows.

$$W = Y_{ij}^u 10_i 10_j 5_H + Y_{ij}^{d,e} 10_i 5_j 5_H + Y_{ij}^{\nu} 1 1_i 5_j 5_H + \frac{1}{2} M_{ij} 1 1_i 1_j + \mu 5_H 5_H .$$  \hspace{1cm} (4)

Since $10$ contains left-handed quark doublet, the diagonalizing matrices of $10$ fields are naively expected as

$$10_i \rightarrow (V_{10})_{ij} 10_j , \hspace{1cm} V_{10} \sim \begin{pmatrix} 1 & \lambda & \lambda^3 \\ \lambda & 1 & \lambda^2 \\ \lambda^3 & \lambda^2 & 1 \end{pmatrix} ,$$  \hspace{1cm} (5)

where $\lambda$ is Cabibbo angle ($\lambda = 0.22$) and we omit the $O(1)$ coefficients. This rotation generates off-diagonal entries of the sfermion masses of $10$ fields as

$$V_{10}^\dagger \begin{pmatrix} m_0^2 \\ m_0^2 \\ m_{30}^2 \end{pmatrix} V_{10} \sim \begin{pmatrix} m_0^2 \\ m_0^2 \\ m_{30}^2 \end{pmatrix} + m_{mix0}^2 ,$$

$$m_{mix0}^2 \sim (m_{30}^2 - m_0^2) \begin{pmatrix} \lambda^6 & \lambda^5 & \lambda^3 \\ \lambda^5 & \lambda^4 & \lambda^2 \\ \lambda^3 & \lambda^2 & 0 \end{pmatrix} ,$$  \hspace{1cm} (6)

at the GUT scale.

In the following, we examine the LFV processes with the above sfermion masses. We use the mass insertion method to estimate the amplitudes for a while. As the slepton mass matrices at the SUSY breaking scale, we adopt the slepton mass matrices given by replacing the $m_0, m_{30},$ and $m_{mix0}$ with $m, m_3,$ and $m_{mix}$, respectively, which are the slepton mass parameters at the SUSY breaking scale. As mentioned in Introduction, we neglect the radiatively induced off-diagonal slepton mass matrices. The weak scale stability requires that $m_3, M_{1/2}, \mu,$ and $A$ must be around the weak scale, but the other parameters, for example, $m,$ can be much larger than the weak scale. In this paper, we often take $m_3, M_{1/2}, \mu, A \ll m.$ For the left-right mixing SUSY breaking parameters, $A,$ we just neglect the contributions in this paper. One reason is that this
contributions are decoupled in the limit $m_3, M_{1/2}$, $\mu$, $A \ll m$, and the other reason is that we would like to examine the model independent parts while the left-right mixing SUSY breaking parameters are strongly dependent on the explicit models. On the other hand, the diagrams (a) and (b) are not decoupled because $m_{\text{mix}}^2$ becomes large in the limit. Therefore, we consider only (a) and (b) for a while. When $\tan \beta$ is large, the diagram (b) which is proportional to $Y_j = \sqrt{2} m_{ej} / v \cos \beta$ is significant, where $v = 246$ GeV. The ratio of (b) and (a) is roughly

$$\frac{\text{Amp}(b)}{\text{Amp}(a)} \sim \tan \beta.$$  

Let us roughly estimate the branching ratio of $\mu \rightarrow e\gamma$ from the diagram (b) which is expected to give the largest contribution. Comparing the diagram for $\mu \rightarrow e\gamma$ with that for $\mu \rightarrow e\nu\bar{\nu}$ ($\text{Br}(\mu \rightarrow e\nu\bar{\nu}) \simeq 100\%$), we can roughly estimate the $\mu \rightarrow e\gamma$ branching ratio as

$$\text{Br}(\mu \rightarrow e\gamma) \simeq \frac{\Gamma(\mu \rightarrow e\gamma)}{\Gamma(\mu \rightarrow e\nu\bar{\nu})} \sim \frac{1}{16\pi^2} \frac{G_F^2}{m_S^4} \left| e(g')^2 \left( \frac{\tan \beta}{m_{\text{mix}}^{(21)}} \right)^2 \right|^2,$$

where $G_F$ is Fermi constant and $m_S$ is typical superparticle mass. For example, if we take $m_S = 400$ GeV, $\tan \beta = 5$, (8) is found as

$$\text{Br}(\mu \rightarrow e\gamma) \sim 10^{-11} \times \mathcal{O}(1) \, .$$  

We find that it is as large as the experimental upper bound ($\text{Br}(\mu \rightarrow e\gamma) < 1.2 \times 10^{-11}$[15]). Since there is no lepton mass dependence in equation (8), it can be applied for the $\tau \rightarrow \mu\gamma$ branching ratio. Substituting $(m_{\text{mix}}^{(32)})$ and $\text{Br}(\tau \rightarrow e\nu\bar{\nu})$ for $(m_{\text{mix}}^{(21)})$ and $\text{Br}(\mu \rightarrow e\nu\bar{\nu})$, respectively, the $\tau \rightarrow \mu\gamma$ branching ratio is found roughly as

$$\text{Br}(\tau \rightarrow \mu\gamma) \sim \left( \frac{\text{Br}(\tau \rightarrow e\nu\bar{\nu})}{\text{Br}(\mu \rightarrow e\nu\bar{\nu})} \right) \frac{\lambda^4}{\lambda^{10}} \times \text{Br}(\mu \rightarrow e\gamma) \sim 10^3 \times \text{Br}(\mu \rightarrow e\gamma) \times \mathcal{O}(1) \, .$$

Then, for the same $m_S$ and $\tan \beta$ as in the above estimation of $\text{Br}(\mu \rightarrow e\gamma)$,

$$\text{Br}(\tau \rightarrow \mu\gamma) \sim 10^{-8} \times \mathcal{O}(1) \, .$$  

The branching ratio of $\tau \rightarrow \mu\gamma$ is also as large as reach of experimental bound ($\text{Br}(\tau \rightarrow \mu\gamma) < 4.5 \times 10^{-8}$[14]). The relation between $\text{Br}(\tau \rightarrow \mu\gamma)$ and $\text{Br}(\tau \rightarrow e\gamma)$,

$$\text{Br}(\tau \rightarrow e\gamma) \sim \lambda^2 \text{Br}(\tau \rightarrow \mu\gamma) \times \mathcal{O}(1) \, .$$
is also an interesting prediction of this scenario. Unfortunately $\tau \rightarrow e\gamma$ process is more
difficult to be observed because of the small branching ratio because the experimental
bound, $\text{Br}(\tau \rightarrow e\gamma) < 1.1 \times 10^{-7}$ [10], is similar to that of $\tau \rightarrow \mu\gamma$ process. Since the
above estimations are very rough, more accurate calculations are necessary. Such accurate
calculations and the results are given in the next section.

Before going to the numerical calculations, we mention about the other source of
LFV. It has been discussed that the loop corrections induce the off-diagonal elements of
left-handed slepton soft masses as

$$ (m^2_{\tilde{l}})_{ij} \simeq -\frac{1}{8\pi^2}(2\tilde{m}_0^2 + m_{H_u}^2)(Y^{\nu\dagger}Y^{\nu})_{ij} \log \frac{M_{\text{mediated}}}{M}, \quad (13) $$

where $M$ and $M_{\text{mediated}}$ are the right-handed neutrino mass scale and the mediation scale
of SUSY breaking, respectively. If

$$ (Y^{\nu\dagger}Y^{\nu})_{23} \geq \lambda^2 \quad \text{or} \quad (Y^{\nu\dagger}Y^{\nu})_{12} \geq \lambda^5, \quad (14) $$

then this loop correction may become sizable. For example, in SO(10) GUT model
with minimal Higgs sector above equality is just hold because of SO(10) GUT relation
$Y^{\nu} = Y^{\nu}$, though not in E$_6$ models due to the smaller Dirac neutrino Yukawa couplings.
Since these contributions are decoupled again in the limit $m_3, M_{1/2}, \mu, A \ll m$, we
neglect this effect in this paper.

In case where $A_{d,e}^{d,e}$ have non-vanishing off-diagonal elements in the $Y^{d,e}$ diagonal basis,
it leads large LFV. The LFV occurs through the diagram (c). The ratio of amplitudes of
diagram (c) and that of (b) is roughly found as

$$ \frac{\text{Amp}(c)}{\text{Amp}(b)} \sim \frac{M_I A^{d,e}_{ij} v \cos \beta}{m_j \tan \beta (m_{\text{mix}}^2)_{ji}}. \quad (15) $$

If $A_{d,e}^{d,e} > \tilde{Y}^{d,e}_{\beta} \tan \beta (m_{\text{mix}}^2)_{ji}/M_I$ is hold, a contribution from diagram(c) is more significant
than (b). As we noted, this contribution is dependent on the explicit models and decoupled
in the limit $m_3, M_{1/2}, \mu, A \ll m$, and therefore, we just neglect this effect in this paper.
When the A-terms are proportional to relevant Yukawa matrices ($A^{d,e} = a_0 Y^{d,e}$) or even when the A-term is vanishing, the double-mass insertion diagram (d) via $\mu$ parameter can contribute the LFV processes. This contribution is included in our calculation in the next section, but it is small. This may be because it is decoupled in the above limit and it is vanishing when $m_3 = m$.  

7
3 The Branching Ratios

Let us discuss the branching ratio of $\tau \rightarrow \mu \gamma$ and $\mu \rightarrow e\gamma$. The amplitude of $l_j \rightarrow l_i \gamma$ is written as

$$T = e^a(q)\bar{u}_i(p-q)i\sigma_{\alpha\beta}q^\beta(A_L^{(ji)}P_L + A_R^{(ji)}P_R)u_j(p) ,$$

where $p$ and $q$ represent the momenta of $l_j$ and photon, respectively. Ignoring a mass of $l_i$ the decay rate is given by

$$\Gamma(l_j \rightarrow l_i \gamma) = \frac{m_{l_j}^3}{16\pi^2}(|A_L^{(ji)}|^2 + |A_R^{(ji)}|^2) .$$

Now we can see an interesting feature in this model. This model says final state lepton tends to have the right-handed chirality. From the operator form [10], we find that chirality flip is necessary with picking up the Yukawa couplings. In this model, only flavor violating coupling in the charged lepton sector is $m_{l_j}$ tends to have the right-handed chirality. From the operator form (16), we find that right-handed stau mass defined as

$$m_{\tilde{\tau}_R} \equiv m_{\tilde{\tau}^R_{1,2}} \equiv m_{\tilde{\tau}^R_1} + m_{\tilde{\tau}^R_2} \cos^2 2\beta \sin^2 \theta_W$$

and the right-handed stau mass defined as $m_{\tilde{\tau}_R} \equiv m_{\tilde{\tau}^R_3} \equiv m_{\tilde{\tau}^R_3} + m_{\tilde{\tau}^R_4} \cos^2 2\beta \sin^2 \theta_W$, which give the

\footnote{Note that the effect of $O(1)$ coefficients can be large as discussed in the previous section. We also neglect a suppression factor ($\sim 15\%$) induced by electromagnetic corrections[17].}

Moreover, we use the observed CKM matrix as the form of unitary matrix for $e_R$ which diagonalizes $Y^q[1]$. Here, only for simplicity, we take the vanishing CP phase. In the above assumption, the number of free parameters which determine the branching ratios is $5 : m$, $m_3$, the higgsino mixing parameter ($\mu$), the $SU(2)_L$ gaugino mass ($M_2$), and the Higgs VEV ratio ($\tan \beta$). In the following, instead of $m$ and $m_3$, we use the first two generation right-handed slepton masses defined as $m_{\tilde{e}_R_{1,2}} \equiv m_{\tilde{e}^R_{1,2}} \equiv m_{\tilde{e}^R_1} + m_{\tilde{e}^R_2} \cos^2 2\beta \sin^2 \theta_W$ and the right-handed stau mass defined as $m_{\tilde{\tau}_R} \equiv m_{\tilde{\tau}^R_3} \equiv m_{\tilde{\tau}^R_3} + m_{\tilde{\tau}^R_4} \cos^2 2\beta \sin^2 \theta_W$, which give the
eigenvalues of the slepton mass matrix in the limit in which the lepton Yukawa couplings are vanishing.

In Fig. 1, we show the dependence of $Br(\tau \rightarrow \mu \gamma)$, $Br(\mu \rightarrow e \gamma)$ on the first two generation right-handed slepton mass. Here, we take $M_2 = 120 \text{ GeV}$, $\mu = 250 \text{ GeV}$, $\tan \beta = 10$, $m_{\tilde{e}_R} = 150 \text{ GeV}$\(^2\). The sign of $\mu$ is taken so that the chargino contribution to the $b \rightarrow s \gamma$ process has the opposite sign for the SM contribution. We can see that the branching ratios become zero at the point where $m_{\tilde{e}_{R1,2}}$ is 150 GeV. This is because the flavor violating source ($m_{\text{mix}}^2$) is vanished, since right-handed slepton masses are universal. Since we do not take account of the slepton LR mixing or the radiatively induced flavor violating source in this paper, it seems that their contributions dominate actually at this region. On the other hand, as we can see in Fig. 1, both branching ratios are not vanishing in the limit $m_{\tilde{e}_{R1,2}} \gg m_{\tilde{e}_{R3}}$. Let us explain the reason, using the mass insertion method. Both $\tau \rightarrow \mu \gamma$ and $\mu \rightarrow e \gamma$ diagrams (a) and (b) include the first or the second generation right-handed slepton in the loop. However, in the limit $m_{\tilde{e}_{R1,2}} \gg m_{\tilde{e}_{R3}}$, the internal lines can be estimated as

\(^2\) This parameter set has been adopted to avoid the weak scale instability in the paper\([13]\) in which we discussed the little hierarchy problem.
for $\tau \rightarrow \mu \gamma$,

$$
\tilde{\tau}_R \rightarrow \frac{(m_{\tilde{\tau}}^2)}{\lambda \tilde{\tau}_R} \sim \frac{1}{m^2_{\tilde{\tau}\tilde{\tau}}} \left( m_{\tilde{\tau}}^2 - m^2 \right) \lambda^2 \frac{1}{m^2_{\tilde{\tau}\tilde{\tau}}} \underset{m \rightarrow \infty}{\longrightarrow} \frac{\lambda^2}{m^2_{\tilde{\tau}\tilde{\tau}}},
$$

(20)

for $\mu \rightarrow e\gamma$. When $m_{\tilde{\nu}_{\tilde{\tau}1,2} \tilde{\nu}_{\tilde{\tau}3}} > m_{\tilde{\nu}_{\tilde{\tau}3}}$, the flavor changing off-diagonal entries become also large. As a result, both transition rates remain finite. From Fig.1, the branching ratios no longer depend on the first two generation masses in $m_{\tilde{\nu}_{\tilde{\tau}1,2}} > 600$ GeV region.

In Figs. 2 and 4, we show the $\mu$ dependence of $Br(\tau \rightarrow \mu\gamma)$ and $Br(\mu \rightarrow e\gamma)$. Here, we take $m_{\tilde{\nu}_{\tilde{\tau}1,2}} = 1000$ GeV and the other parameters are taken as in the previous one. We find that around $\mu \sim 20, -1000$ GeV the branching ratios become very small. To understand this behavior, we should remind that neutralino amplitude consists of two parts. One is proportional to $m_{\tilde{\nu}_l}$, the other is proportional to $M_{\tilde{\nu}_l}$, they correspond to diagram (a) and diagram (b), respectively. In Figs. 3 and 5, the dotted line represents the amplitude which are proportional to $m_{\tilde{\nu}_l}$ and the solid line represents the amplitude which is proportional to $M_{\tilde{\nu}_l}$. As we can see from these figures, the $m_{\tilde{\nu}_l}$ part depends hardly on $\mu$. This is because this part comes mainly from the diagram (a) in which higgsinos do not contribute. On the other hand, the $M_{\tilde{\nu}_l}$ part which comes mainly from the diagram (b) depends on $\mu$. This part changes its sign from $\mu < 0$ to $\mu > 0$ and is decreasing as increasing $\mu$ due to the decoupling. Basically, contribution of diagram (b) is larger than that of diagram (a) due to tan $\beta$ enhancement. However, when diagram (b) changes its sign, or it goes to decouple as increasing $|\mu|$, there are two points where the magnitude of diagram (b) becomes smaller than that of diagram (a). If each diagrams have different sign in these points, they are cancelled. Now, we could understand the vanishing point in Figs. 2 and 4. Note that the cancellation happens mainly in the $\mu < 0$ region. Consequently, the branching ratios do not strongly depend on $\mu$ in the positive $\mu$ region where the chargino contribution to $b \rightarrow s\gamma$ has opposite sign for the SM contribution and the charged Higgs contribution to $b \rightarrow s\gamma$.

In Figs. 6, we show the $M_2$ dependence of the branching ratios when $\mu = 250$ GeV. Here, we take the same parameters as those in the previous figures. We can see the point around $M_2 \sim 0$ GeV in which the branching ratios are vanishing. This is because of the cancellation between the contributions from the diagram (a) and (b) as in Figs. 2 and 4. The region with $M_2 < 0$ and $\mu > 0$ corresponds to the region $M_2 > 0$ and $\mu < 0$.

Figs. 7 and 8 show the $\tau \rightarrow \mu\gamma$ and $\mu \rightarrow e\gamma$ branching ratios for tan $\beta$ and right-handed stau mass when $M_2 = 120$ GeV. We take the other parameters to be the same as in the previous figures. In Fig. 7, the dashed line represents $Br(\tau \rightarrow \mu\gamma) = 4.5 \times 10^{-8}$ and the left side of the dashed line is excluded by current experiment. The solid lines represents $Br(\tau \rightarrow \mu\gamma) = 1 \times 10^{-8}, 10^{-9}, 10^{-10}, 10^{-11}$ from the up-left side. It is found that if right-handed stau mass is about 100 GeV, tan $\beta$ cannot be taken larger than 9. The region where $4.5 \times 10^{-8} > Br(\tau \rightarrow \mu\gamma) > 5 \times 10^{-9}$ is the target region of the B-factory or super B-factory[18]. If the right-handed stau is light ($m_{\tilde{\nu}_{\tilde{\tau}3}} < 200$ GeV, when
Figure 2: $\mu$ dependence of $Br(\tau \to \mu\gamma)$

Figure 3: The solid line represents the $\mu$ dependence of the $\tau \to \mu\gamma$ neutralino amplitude which is proportional to $m_{\tilde{\chi}_0}$, and the dotted line represents the $\mu$ dependence of the $\tau \to \mu\gamma$ neutralino amplitude which is proportional to $m_\tau$.

Figure 4: The $\mu$ dependence of $Br(\mu \to e\gamma)$

Figure 5: The solid line represents the $\mu$ dependence of the $\mu \to e\gamma$ neutralino amplitude which is proportional to $m_{\tilde{\chi}_0}$, and the dotted line represents the $\mu$ dependence of the $\mu \to e\gamma$ neutralino amplitude which is proportional to $m_\mu$. 
tan $\beta \sim 10$), the $\tau \to \mu \gamma$ process can be discovered at the B factory or super B-factory. In Fig. 8, the solid lines represent $Br(\mu \to e\gamma) = 10^{-11}, 10^{-12}, 10^{-13}, 10^{-14}, 10^{-15}$ from the up-left side and the dashed line represents the current limit $Br(\mu \to e\gamma) < 1.2 \times 10^{-11}$. The region $10^{-11} > Br(\mu \to e\gamma) > 10^{-14}$ is the target region of the MEG experiment\cite{19}. Thus, we find if the right-handed stau is light ($m_{\tilde{\tau}^R} < 420$ GeV, when $\tan \beta \sim 10$), $\mu \to e\gamma$ may be discovered at the MEG experiment. We calculated these figures with the negative $\mu = -250$ GeV. The results are similar to the Figs. 7 and 8. However, when the $\mu$ is negative, the chargino contribution to the $b \to s\gamma$ process has the same sign as the SM contribution and the charged Higgs contribution. Therefore, other large contribution to the $b \to s\gamma$ process with opposite sign is required.

Comparing these figures, we find that the $\tau \to \mu \gamma$ process gives more severe constraints to this scenario than the $\mu \to e\gamma$ process at present. Before the MEG experiment finds the signal of the $\mu \to e\gamma$, the $\tau \to \mu \gamma$ events can be found in the B-factory.

4 Conclusion

In this paper, we have analyzed the lepton flavor violating $\tau \to \mu \gamma$ and $\mu \to e\gamma$ processes in SUSY GUT model in which the third generation sfermion masses, $m_3$ of 10 of SU(5) have different masses from the others, $m$. Such mass spectrum is consistent with the present constraints from the various FCNC processes. And it is interesting that such mass spectrum is naturally derived from the GUT models with $E_6 \times$ Horizontal Symmetry.

This mass spectrum allowed us to take very large value for $m$ without destabilizing the weak scale in the MSSM, because stop masses are determined by $m_3$. We have considered a situation where $m_3$ is of order the weak scale while $m$ is larger than the weak scale. In this case, the LFV decay rates are determined mainly by the right-handed stau mass and $\tan \beta$. Especially, the branching ratios of $\tau \to \mu \gamma$ and $\mu \to e\gamma$ strongly depend on the right-handed stau mass. This means that this type of soft mass matrix can be tested by
Figure 7: Dependence of $Br(\tau \to \mu \gamma)$ on $\tan \beta$ and $m_{\tilde{e}_{R3}}(\mu = 250 \text{ GeV})$. The solid lines represent $Br(\tau \to \mu \gamma) = 10^{-8}, 10^{-9}, 10^{-10}, 10^{-11}$ from the up-left side to the down-right side. The dashed line represents the current bound.

Figure 8: Dependence of $Br(\mu \to e \gamma)$ on $\tan \beta$ and $m_{\tilde{e}_{R3}}(\mu = 250 \text{ GeV})$. The solid lines represent $Br(\mu \to e \gamma) = 10^{-11}, 10^{-12}, 10^{-13}, 10^{-14}, 10^{-15}$ from the up-left side to the down-right. The dashed line represents the current bound.
checking the relation among the LFV decay rates and the right-handed stau mass which may be measured in the direct search, though the ambiguity due to the $O(1)$ coefficients still exists. As we can see from Figs. 7 and 8, if the right-handed stau is lighter than 420 GeV (when $\tan \beta \sim 10$), $\mu \rightarrow e\gamma$ process may be discovered at the MEG experiment. It may be interesting that the B-factory can find the $\tau \rightarrow \mu\gamma$ events before the MEG experiment find the $\mu \rightarrow e\gamma$ events because the present constraints from $\tau \rightarrow \mu\gamma$ is more severe than that from the $\mu \rightarrow e\gamma$ process.

Moreover, this model provides some interesting predictions. First, this model says that the final state lepton tends to have the right-handed chirality, because the intermediate state must have the right-handed chirality to pick up the flavor violating mass matrix entries. On the other hand, the LFV processes induced radiatively via large Dirac neutrino Yukawa interactions predicts an opposite chirality (left-handed) for the final state lepton. This difference can be checked by measuring the angular distribution of the final lepton for the initial lepton’s spin. Second, this model predicts several relations among $\tau \rightarrow \mu\gamma$, $\mu \rightarrow e\gamma$, and $\tau \rightarrow e\gamma$ as $Br(\tau \rightarrow \mu\gamma) \sim 10^3 \times [O(1)]^4 Br(\mu \rightarrow e\gamma) \sim 20 \times [O(1)]^4 Br(\tau \rightarrow e\gamma)$. This enhancement factor of the former relation can be understood as $Br(\tau \rightarrow e\nu\bar{\nu}) \times \lambda^4 / \lambda^{10}$ and that of the latter as $\lambda^{-2}$. It is important to test these predictions in future experiments.

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Appendix

In this appendix, we give our notation and conventions adopted in Section 3, which are basically the same as in the papers [20, 21].

First we consider the sfermions. Below the weak scale, the mass matrix of the charged slepton is given in the super-CKM basis as

$$\mathcal{L}_m \ni (\tilde{e}_L^\dagger \tilde{e}_R^\dagger) m^2_{\tilde{e}} \begin{pmatrix} \tilde{e}_L \\ \tilde{e}_R \end{pmatrix},$$

$$m^2_{\tilde{e}} = \begin{pmatrix} m^2_{\tilde{\nu}_5} + m^2_Z \cos^2 2\beta (-\frac{1}{2} + \sin^2 \theta_W) + m^2_e & -m_e (A_e + \mu \tan \beta) \\ -m_e (A_e + \mu \tan \beta) & V^\dagger_{10} m^2_{\tilde{e}_{10}} V_{10} + m^2_Z \cos^2 2\beta \sin^2 \theta_W + m^2_e \end{pmatrix},$$

(24)

where $m^2_{\tilde{\nu}_5}$ and $m^2_{\tilde{e}_{10}}$ are slepton soft mass matrices given in Eq. (3) at the low energy, $V_{10}$ is a diagonalizing matrix given in Eq. (5), and $m_e$ is the diagonal charged lepton mass matrix. Here we assumed that the $A$-term is proportional to the Yukawa matrix. We define the $6 \times 6$ unitary matrix $\Gamma_{e}$ which rotates the left(right)-handed slepton fields into mass eigenstate $\tilde{e}_k$ ($k = 1, \ldots , 6$) as

$$\Gamma_{e}(m^2_{\tilde{e}}) \Gamma_{e}^\dagger = \text{(diagonal)}, \quad \tilde{e}_{L(R)} = \Gamma_{e L(R)}^\dagger \tilde{e},$$

where $6 \times 3$ matrices $\Gamma_{e L(R)}$ are defined as

$$\Gamma^k_{eL} = \Gamma^k_{e}, \quad \Gamma^k_{eR} = \Gamma^k_{e} \lambda^3.$$
Now we turn to the neutralinos. The mass term of the neutralino sector is given by

\[
- \mathcal{L}_m \ni \frac{1}{2} \left( \tilde{\gamma} \tilde{\gamma} \tilde{Z} \tilde{H}_d^0 \tilde{H}_u^0 \right) \cdot \mathbf{M}_{\tilde{\chi}^0} \left( \begin{array}{c} \tilde{\chi}_0^0 \\ \tilde{\chi}_1^0 \\ \tilde{\chi}_2^0 \\ \tilde{\chi}_3^0 \\ \tilde{\chi}_4^0 \end{array} \right) + \text{h.c.},
\]

(26)

where

\[
\mathbf{M}_{\tilde{\chi}^0} = \begin{pmatrix}
M_1 \cos^2 \theta_W + M_2 \sin^2 \theta_W & \cos \theta_W \sin \theta_W (M_2 - M_1) & 0 & 0 \\
\cos \theta_W \sin \theta_W (M_2 - M_1) & M_1 \sin^2 \theta_W + M_2 \cos^2 \theta_W & m_Z \cos \beta & -m_Z \sin \beta \\
0 & m_Z \cos \beta & 0 & -\mu \\
0 & -m_Z \sin \beta & -\mu & 0
\end{pmatrix}.
\]

(27)

This neutralino mass matrix can be diagonalized by a real orthogonal matrix \( N \):

\[
\mathbf{M}_{\tilde{\chi}^0} N^T = \text{(diagonal)}.
\]

(28)

The mass eigenstates \( \tilde{\chi}_i^0 \) \((i = 1, \ldots, 4)\) are given by

\[
\begin{pmatrix}
\tilde{\chi}_1^0 \\
\tilde{\chi}_2^0 \\
\tilde{\chi}_3^0 \\
\tilde{\chi}_4^0
\end{pmatrix} = N
\begin{pmatrix}
\tilde{\gamma} \\
Z \\
H_d^0 \\
H_u^0
\end{pmatrix}.
\]

(29)

We use the following vertices.

\[
\begin{align*}
\varepsilon_i & \to \tilde{\chi}_j^0 & = & - i g \left[ (\sqrt{2} C_{0eL}^{jki} + H_{0eR}^{jki}) P_L - (\sqrt{2} C_{0eR}^{jki} - H_{0eL}^{jki}) P_R \right] \\
\tilde{\chi}_i & \to \varepsilon_k & = & - i g \left[ (\sqrt{2} C_{0eL}^{rjki} + H_{0eR}^{rjki}) P_R - (\sqrt{2} C_{0eR}^{rjki} - H_{0eL}^{rjki}) P_L \right],
\end{align*}
\]

(30, 31)

where

\[
C_{0eL}^{jki} \equiv \left[ - \sin \theta_W N^{j1*} + \frac{1}{\cos \theta_W} (- \frac{1}{2} + \sin^2 \theta_W) N^{j2*} \right] \Gamma_{eL}^{ki},
\]

(32)

\[
C_{0eR}^{jki} \equiv \left[ - \sin \theta_W N^{j1*} + \frac{\sin^2 \theta_W}{\cos \theta_W} N^{j2*} \right] \Gamma_{eR}^{ki},
\]

(33)

\[
H_{0eL}^{jki} \equiv N^{j3*} (\Gamma_{0eL} Y_e)^{ki}/g,
\]

(34)

\[
H_{0eR}^{jki} \equiv N^{j3*} (\Gamma_{0eR} Y_e)^{ki}/g.
\]

(35)

Finally, we show the functions \( F_2 \) and \( F_4 \) which appear in eq. (18) as

\[
F_2(x) = \frac{1}{12(x-1)^4} \left( 2x^3 + 3x^2 - 6x + 1 - 6x^2 \log x \right),
\]

\[
F_4(x) = \frac{1}{2(x-1)^3} \left( x^2 - 1 - 2x \log x \right).
\]

(36)
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