Atmospheric neutrino flux at INO, South Pole and Pyhäsalmi

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Abstract

We present the calculation of the atmospheric neutrino fluxes for the neutrino experiments proposed at INO, South Pole and Pyhäsalmi. Neutrino fluxes have been obtained using ATMNC, a simulation code for cosmic ray in the atmosphere. Even using the same primary flux model and the interaction model, the calculated atmospheric neutrino fluxes are different for the different sites due to the geomagnetic field. The prediction of these fluxes in the present paper would be quite useful in the experimental analysis.

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I. INTRODUCTION

The study of neutrino physics with atmospheric neutrinos has a long history with the first observations of muons produced by $\nu_\mu$ in deep underground laboratories of Kolar Gold Field (KGF) mines in India [1] and East Rand Proprietary Mines (ERPM) in South Africa [2]. It was the Kamiokande [3], IMB [4] and some other atmospheric neutrino experiments [5] which gave a clear evidence of a deficit in the atmospheric muon neutrino flux. With the Super-Kamiokande [6] experiment, it is now well established that atmospheric neutrinos do oscillate. Both theoretically and experimentally lots of activities are going on to precisely determine neutrino oscillation parameters and experiments are planned with atmospheric as well as with the accelerator, reactor and solar neutrinos.

India is going to establish a neutrino observatory at the Theni district of Tamilnadu [7]. This India-based Neutrino Observatory (INO) is proposed to be installed at $9^\circ 96^\prime 7^\prime\prime$N, $77^\circ 26^\prime 7^\prime\prime$E, and their primary aim is to study atmospheric neutrinos in a 1300 meters deep cave. The detector that is planned to be used is a magnetized iron calorimeters (ICAL) of 50kT. At the South Pole, PINGU (Precision IceCube Next Generation Upgrade) is proposed as the upgrade version of IceCube (-90°, 0°) [8] to observe atmospheric neutrino at lower energies by increasing the optical modules many times of the present setup, under the surface of the ice. Another new generation underground neutrino experiment facility called LAGUNA (Large Apparatus studying Grand Unification and Neutrino Astrophysics) is proposed at Pyhasalmi Mine [9] in Finland, which is among the deepest mines in Europe at $63^\circ 39^\prime$N, $26^\circ 02^\prime$E.

In this paper, we have calculated atmospheric neutrino fluxes for these three sites in a 3D scheme using ATMNC (ATmospheric Muon Neutrino Calculation) code [10–12] for the cosmic ray propagation in atmosphere with JAM, which is used in PHITS (Particle and Heavy-Ion Transport code System) [13], in the hadronic interaction at lower energies (< 32 GeV). The JAM interaction model agrees with the HARP experiment [14] a little better than DPMJET-III [15]. Earlier ATMNC code has been applied to the study of muon flux at several altitudes, at sea level, mountain altitude, and at balloon altitudes, where accurate measurements exist. The Monte Carlo generator with JAM shows a better agreement than the former one without JAM. Then it is applied to the calculation of atmospheric neutrino flux for several sites as the GranSasso, SNO, Kamioka and others [10–12].
In spite of using the same primary flux model and the interaction model for the different sites, the calculated atmospheric neutrino fluxes are different due to the geomagnetic field. The geomagnetic field affects cosmic rays both inside and outside of the atmosphere. First, it acts as a filter for low energy cosmic rays, and secondly, it deflects the charged particles in the atmosphere. These two effects are mainly controlled by the horizontal component of the geomagnetic field. It would be interesting to study the atmospheric neutrino flux for the three sites with different position in the geomagnetic field. In Fig. I, we show the strength of the horizontal component of geomagnetic field obtained using IGRF2010 model [16] with the position of these sites. It can be seen that the INO site is close to the region where the strength of the horizontal component of geomagnetic field is the largest on the earth. The South Pole is close to the magnetic pole, where the horizontal component is zero. At Pyhäsalmi mine, the horizontal component of geomagnetic field is also small but not zero as it is little far away from the magnetic pole.

We proceed as follows. In section-II, we present the main features of the calculation scheme and in section-III, the results of the atmospheric neutrino fluxes have been shown and discussed. Finally, in section-IV, we summarize the results and conclude our findings.

II. CALCULATION SCHEME

The scheme for calculating the atmospheric neutrino fluxes has been discussed in detail in the earlier work [10-12]. We present here the main features. We use the primary flux model based on AMS [17, 18] and BESS [19, 20] data. We use IGRF2010 [16] model for the geomagnetic field. For the atmosphere model, we use NRLMSISE-00 [21] instead of US-standard76 [22], which was used in our earlier works [10, 12]. Actual calculation is carried out in the Cartesian coordinate system which has the origin at the center of the Earth, with the Z-axis extending to the north pole, and we consider the surface of the Earth to be a sphere with a radius of \( R_e = 6378.180 \) km. However, the position on the Earth is well represented by the spherical polar coordinate system \((r, \theta, \phi)\) with \( r = R_e \) which is related to the Cartesian coordinate system by

\[
x = R_e \sin \theta \cos \phi, \quad x = R_e \sin \theta \sin \phi \quad \text{and} \quad z = R_e \cos \theta.
\]

The local coordinate system at the detector is constructed based on this polar coordinate
system. The direction of the x-axis is in the increasing direction of \( \theta \), the direction of the y-axis is in the increasing direction of \( \phi \), and the direction of the z-axis is in the increasing direction of \( r \). Therefore, the azimuth angle is measured counterclockwise from south in the local coordinate system. In addition to the surface of the Earth, we assume three more spheres; the injection sphere, the simulation sphere, and the escape sphere. We have taken the radius of the injection sphere as \( R_{\text{inj}} = R_e + 100 \text{km} \), and the radius of simulation sphere and the escape sphere are taken to be \( R_{\text{esc}} = R_{\text{sim}} = 10 \times R_e = 63781.80 \text{ km} \).

Cosmic rays are sampled on the injection sphere uniformly towards the inward direction, following the given primary cosmic ray spectra. Before they are fed to the simulation code for the propagation in air, they are tested to determine whether they pass the rigidity cutoff or not. For a sampled cosmic ray, the “history” is examined by solving the equation of motion in the negative time direction. When the cosmic ray reaches the escape sphere without touching the injection sphere again in the inverse direction of time, the cosmic ray can pass through the magnetic barrier following its trajectory in the normal direction of time. The propagation of cosmic rays is simulated in the space between the surface of Earth and the simulation sphere.

We use the JAM interaction model for hadronic interactions below 32 GeV, as this shows a better agreement with the HARP experiment [14] and it agrees with the observed muon flux at sea level, at mountain altitudes and at balloon altitudes. For energies above 32 GeV, we use DPMJET-III [15] interaction model. We have checked the smooth interpolation when switching from the JAM model to the DPMJET-III interaction model.

III. RESULTS AND DISCUSSIONS

In this section, we present the results of simulation for the atmospheric neutrinos at INO, South Pole and Pyhäsalmi sites. First we present the results for the atmospheric neutrino fluxes as a function of azimuthal angle \( \phi \). These results are presented for \( \nu_\mu \), \( \bar{\nu}_\mu \), \( \nu_e \) and \( \bar{\nu}_e \) for (anti)neutrinos of 3.2 GeV. In Fig. 2 we present the results for the INO site, in Fig. 3 the results are presented for the South Pole site and in Fig. 4 the results are presented for the Pyhäsalmi site at \( E_\nu = 3.2 \text{ GeV} \). In these figures we show the variation of atmospheric neutrino flux as the function of the azimuthal angle averaging them over the five zenith angle ranges, \( 1 > \cos \theta > 0.6, \ 0.6 > \cos \theta > 0.2, \ 0.2 > \cos \theta > -0.2, \ -0.2 > \cos \theta > - \)
FIG. 1: Magnitude of the horizontal component of geomagnetic field in IGRF2010 model. Square stands for the position of India-based Neutrino Observation (INO) site, diamond for the Pyhäsalmi mines, and bottom bar for the South Pole.

0.6 and -0.6 $> \cos \theta > -1$. We find that the variation of the atmospheric neutrino flux has a complex structure at low (anti)neutrino energies, due to the rigidity cutoff and muon bending in the geomagnetic field. This variation remains almost the same for the near horizontal direction even above 10 GeV. Due to the high rigidity cutoff at the INO site this variation is more complex than the other two sites discussed here and for the South Pole site this variation is the least.

Furthermore, the variation of upward going neutrinos is much more complicated than the variation of downward going neutrinos. This is due to the fact that the upward-going neutrinos are produced in wide area on the Earth, and there are large variation of rigidity cutoff and geomagnetic field. On the other hand, the downward going neutrinos are produced just above the detector.

In Figs. 5, 6 and 7 we present the results for the atmospheric neutrino fluxes as a function of the zenith angle after averaging over all the azimuthal angles. The results are presented
FIG. 2: The azimuthal angle dependence of atmospheric neutrino flux, averaged over zenith angle bins of $1 > \cos \theta > 0.6$ (solid line), $0.6 > \cos \theta > 0.2$ (long dashed), $0.2 > \cos \theta > -0.2$ (short dashed), $-0.2 > \cos \theta > -0.6$ (dashed-dotted), and $-0.6 > \cos \theta > -1$ (dashed double-dotted), calculated for the INO site at (anti)neutrino energy $E=3.2$GeV.

for neutrino energy of 1GeV, 3.2GeV and 10GeV respectively, and for the three sites viz. INO, South Pole and Pyhäsalmi in each of these figures. At 1 GeV, there are large up-down asymmetries in the atmospheric neutrino flux at all the three sites. The downward going neutrino flux is larger at the South pole and Pyhäsalmi sites, while upward going neutrino flux is larger at the INO site due to the different rigidity cutoff. These asymmetries decrease with the increase in neutrino energy, and almost disappear at 10 GeV. However, there appears an up-down asymmetry at South Pole, due to the difference in the observation altitude.

We note that the horizontal/vertical flux ratio for the INO site is much smaller than for the other sites even at 3.2 GeV. This could be understood by the fact that the rigidity cutoff still affect the neutrino flux at 3.2 GeV at the INO site, and the rigidity cutoff is more effective in the horizontal direction.
FIG. 3: Same as Fig. 2 at (anti)neutrino energy $E=3.2\text{GeV}$ for the South Pole site.

FIG. 4: Same as Fig. 2 at (anti)neutrino energy $E=3.2\text{GeV}$ for the Pyhäsalmi site.
FIG. 5: The zenith angle dependence of atmospheric neutrino flux at E=1GeV, averaged over all azimuthal angles calculated for INO, South Pole and Pyhäsalmi sites. Here θ is the arrival direction of the neutrino, with \( \cos \theta = 1 \) for vertically downward going neutrinos, and \( \cos \theta = -1 \) for vertically upward going neutrinos.

In Fig. 8 we have shown proton spectra which produce neutrino above 3.2 GeV, from the near vertical \( (1 > \cos \theta_{\text{zenith}} > 0.4) \) and near horizontal \( (0.2 > \cos \theta_{\text{zenith}} > -0.2) \) directions for the INO site, with effectively no rigidity cutoff site (SNO [23]) and intermediate rigidity cutoff site (SK [6]). On comparing the proton spectra for these sites, it may be noticed that the rigidity cutoff works more efficiently for the near horizontal direction than for the near vertical direction, especially for the INO site [7]. The rigidity cutoff for downward going neutrino at South pole [8] and Pyhäsalmi sites [9] are effectively the same as that of SNO site [23].

In Fig. 9, we present the results for the atmospheric neutrino spectra averaged over zenith and azimuth angles, for (anti)neutrino energies from 0.5 GeV to 10 GeV, for the INO [7], South Pole [8] and Pyhäsalmi [9] sites. We find that when the neutrino flux is integrated over all the angles, the difference in the flux at the South Pole and Pyhäsalmi sites which
FIG. 6: Same as Fig.5 at E=3.2GeV.

FIG. 7: Same as Fig.5 at E=10GeV.
FIG. 8: The spectra of protons which create the neutrino above 3.2 GeV from the near vertical (1 > cos θ_{zenith} > 0.4, left panel) and near horizontal (0.2 > cos θ_{zenith} > −0.2, right panel) directions at effectively no rigidity cutoff site (SNO [23]), intermediate rigidity cutoff site (SuperK [6]) and at the INO site [7].

FIG. 9: Atmospheric neutrino flux sum over all zenith and azimuthal angles for the INO, South Pole and Pyhäsalmi sites. These results are summed over all the flavors of neutrinos viz. ν_μ + ¯ν_μ + ν_τ + ¯ν_τ.

appeared in Figs. 5, 6 and 7, disappears. Due to the strong effect of the horizontal component of the geomagnetic field atmospheric neutrino flux at the INO site is almost 30% smaller at 1GeV, than the flux at the two other sites discussed here, while this difference becomes smaller with the increase in the neutrino energy, for example, at 3GeV, this difference is
10%, but the flux reduces almost by a factor of 20 as compared to the flux at 1GeV.

IV. SUMMARY AND CONCLUSION

We have studied the atmospheric neutrino flux for the INO, South Pole and Pyhäsalmi sites using ATMNC with JAM interaction code below 32 GeV. We find that the atmospheric neutrino flux is quite different in nature particularly at low and intermediate energies, depending on the position in the geomagnetic field, and the strength of the horizontal component of the geomagnetic field is a good measure of the deviation in the fluxes at the different sites. Especially, the difference of the zenith angle dependence of the atmospheric neutrino flux is important in the analysis of the neutrino oscillation. The difference is large at lower energies up to the neutrino energies of a few GeV. These results would be useful in the analysis of the atmospheric neutrino experiments proposed at these sites.

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