Pressure dependence of coherence-incoherence crossover behavior in KFe$_2$As$_2$ observed by resistivity and $^{75}$As-NMR/NQR

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We present the results of $^{75}$As nuclear magnetic resonance (NMR), nuclear quadrupole resonance (NQR), and resistivity measurements in KFe$_2$As$_2$ under pressure ($p$). The temperature dependence of the NMR shift, nuclear spin-lattice relaxation time ($T_1$) and resistivity show a crossover between a high-temperature incoherent, local-moment behavior and a low-temperature coherent behavior at a crossover temperature ($T^*$). $T^*$ is found to increase monotonically with pressure, consistent with increasing hybridization between localized 3d orbital-derived bands with the itinerant electron bands. No anomaly in $T^*$ is seen at the critical pressure $p_c = 1.8$ GPa where a change of slope of the superconducting (SC) transition temperature $T_c(p)$ has been observed. In contrast, $T_c(p)$ seems to correlate with antiferromagnetic spin fluctuations in the normal state as measured by the NQR $1/T_1$ data, although such a correlation cannot be seen in the replacement effects of A in the AFe$_2$As$_2$ ($A=K, Rb$, Cs) family. In the superconducting state, two $T_1$ components are observed at low temperatures, suggesting the existence of two distinct local electronic environments. The temperature dependence of the short $T_{1s}$ indicates nearly gapless state below $T_c$. On the other hand, the temperature dependence of the long component $1/T_{1l}$ implies a large reduction in the density of states at the Fermi level due to the SC gap formation. These results suggest a real-space modulation of the local SC gap structure in KFe$_2$As$_2$ under pressure.

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I. INTRODUCTION

The iron-based superconductors (SCs) continue to be the focus of intense research in condensed matter physics, due to their unique interplay of magnetic, orbital and charge degrees of freedom [1,2]. Among the iron-based SCs, the heavily hole-doped iron-pnictide superconductor KFe$_2$As$_2$, with a SC transition temperature of $T_c \sim 3.5$ K, shows several unique properties. The Sommerfeld coefficient ($\gamma \sim 102$ mJ/molK$^2$) is significantly enhanced, and the magnetic susceptibility exhibits a broad peak around 100 K [3]. Nuclear magnetic resonance (NMR) spin-lattice relaxation rates ($1/T_1$) are strongly enhanced, evidencing antiferromagnetic spin fluctuations. Curie-Weiss fits to the NMR data have demonstrated the proximity of KFe$_2$As$_2$ to a quantum critical point (QCP) [4,5]. These results indicate a heavy quasiparticle effective mass and strong electronic correlations [6,7]. Recent NMR investigations have also pointed out the importance of ferromagnetic spin correlations in this material [5].

Furthermore, the SC properties of KFe$_2$As$_2$ are also unique. Whereas two full SC gaps are reported in the hole-doped series Ba$_{1-x}$K$_x$Fe$_2$As$_2$ for $x < \sim 0.8$ [10], a nodal SC gap structure in KFe$_2$As$_2$ ($x = 1$) has been suggested by several experiments [11,12]. A large full gap accompanied by several very small gaps has also been proposed based on specific heat measurements [17]. In addition, $T_c$ shows non-monotonic behavior under pressure, with a minimum at $p_c \sim 1.8$ GPa, which has been suggested to be caused by a change in the SC gap structure [13,20]. Measurements of the pressure dependence of the upper critical field $H_{c2}$ suggested the appearance of a $k_z$-modulation of the SC gap above $p_c$ [20].

Analogous behavior has also been found in the related alkali metal compounds RbFe$_2$As$_2$ and CsFe$_2$As$_2$ [21–27], which show even greater mass enhancements with $\gamma \sim 127$ mJ/molK$^2$ and $\gamma \sim 184$ mJ/molK$^2$, respectively [28]. The unusual properties of the AFe$_2$As$_2$ ($A=K, Rb$, Cs) family have been pointed out [6,28,29] to be quite similar to $f$-electron heavy fermion materials [30,31], which display a crossover between a high-temperature incoherent, local-moment behavior and a low-temperature coherent behavior, with the crossover occurring at a temperature $T^*$. In this picture, the importance of dual role of Fe $d$ electrons has been pointed out theoretically [32,33] where the two aspects of the itinerant and localized electrons may originate from different 3d orbitals of the iron ions. Recently, experimental [29,34] and theoretical [6] studies suggest that the bands derived from the Fe 3d$_{xy}$ orbitals would play the role of the local moments. This orbital-selective localization is due to the strong Hund coupling in these materials [35].

Recent NMR measurements have pointed out a possible $d$-electron heavy fermion behavior in the AFe$_2$As$_2$...
(A = K, Rb, Cs) family at ambient pressure \[28\]. \(T^\ast\) is reported to increase from 85 K for Cs, to 125 K for Rb and to 165 K for KFe\(_2\)As\(_2\). Thermal expansion measurements on this family also find the lowest \(T^\ast\) for Cs and highest \(T^\ast\) for K, although the reported crossover temperatures are lower \[30\]. Since the so-called chemical pressure effects would increase when one moves from Cs to Rb to K due to the decrease in size of the alkali metal ion, this suggests that \(T^\ast\) increases with increasing the chemical pressure. Furthermore, two empirical relationships involving \(T^\ast\) have been discussed \[28\]. First, the superconducting transition temperature \(T_c\) is generally proportional to \(T^\ast\), that is \(T_c \propto T^\ast\), reflecting the correlation of \(T_c\) to local magnetic coupling \(J\) as pointed out in Ref. \[27\] in the context of \(f\)-electron heavy fermion SCs. Second, the Sommerfeld coefficient \(\gamma\), and thus the effective mass \(m^*\), is inversely proportional to \(T^\ast\), that is \(\gamma^{-1} \propto T^\ast\) (see also Ref. \[6\]).

The \(T_c \propto T^\ast\) relationship for the AFe\(_2\)As\(_2\) (A = K, Rb, Cs) naively suggests that the non-monotonic behavior of \(T_c\) in these materials under pressure could be due to a non-monotonic behavior of \(T^\ast\) under pressure. This motivates an experimental investigation of the relationship between \(T_c\) and \(T^\ast\) under pressure. Here, we have carried out NMR and nuclear quadrupole resonance (NQR) measurements under high pressure up to 2.1 GPa and resistivity measurements up to ~5 GPa in order to investigate the pressure dependence of \(T^\ast\) and to test its relationship with \(T_c\). Based on the NMR and resistivity data, we find that \(T^\ast\) increases monotonically with increasing pressure with no anomaly associated with crossing \(p_c \sim 1.8\) GPa. These results indicate that \(T^\ast\) is not the primary driver of the pressure dependence of \(T_c\) in KFe\(_2\)As\(_2\). On the other hand, \(1/T_1\) measurements demonstrate that spin fluctuations are suppressed with increasing pressure up to the \(p_c\) and then start to be enhanced above \(p_c\), suggesting that \(T_c\) is related to spin fluctuations in the normal state. In the superconducting state, two-component NQR relaxation is observed below \(T = 1\) K, suggesting real space variation of the superconducting gap structure. One of the two components, the short \(T_1\) component, shows no change in the slope of \(1/T_1\) across \(T_c\) above 1.5 GPa, indicating these nuclei see a gapless local electronic environment in the SC state under these pressure conditions. Only the second component, the long \(T_1\) component, shows a large reduction of the density of states at the Fermi energy due to the SC gap.

**II. EXPERIMENTAL DETAILS**

Highly pure KFe\(_2\)As\(_2\) crystal sample was obtained by recrystallization of pre-reacted KFe\(_2\)As\(_2\) polycrystalline powder in KAs flux as follows. KFe\(_2\)As\(_2\) polycrystalline powder was prepared by annealing a stoichiometric mix-
with their axes perpendicular to each other to avoid interference between coils.

The single-crystal electrical resistivity measurements were performed using the four-probe method with current in the ab plane. Pressure was applied at room temperature using a modified Bridgman cell with a 1:1 mixture of n-pentane:isopentane as a pressure medium, with the pressure determined using the superconducting transition of Pb.

III. RESULTS AND DISCUSSION

A. Tc and critical pressure

The superconducting transition temperature $T_c$ of the KFe$_2$As$_2$ powder was determined by measuring the $T$ dependence of the NMR coil tank circuit resonance frequency, $f(T)$, under zero magnetic field. The frequency $f$ is a measure of the ac-susceptibility $\chi_{ac}(\omega_{\text{NMR}})$ since $f = 1/2\pi\sqrt{LC}$ and $L = L_0(1 + \chi_{ac})$. The onset of the Meissner effect therefore results in a sharp change of $f(T)$ as shown in the inset of Fig. 1. At ambient pressure, we find $T_c \approx 3.3$ K, as expected. The pressure dependence of $T_c$ is shown in Fig. 1 together with the data reported previously. $T_c$ decreases with $p$ below the critical pressure $p_c \approx 1.8$ GPa with a rate of 0.97 K/GPa, while $T_c$ shows weak pressure dependence above $p_c$.

B. NMR spectrum

Figure 2 shows a representative field-swept NMR spectrum of the KFe$_2$As$_2$ powder measured at 10 K and $p = 1.9$ GPa. The spectrum is typical for an $I = 3/2$ nucleus in a powder sample with Zeeman interaction greater than quadrupole interaction. A central transition is flanked by two satellite lines split by the quadrupole interaction of the As nucleus with the local electric field gradient (EFG). In addition, the central transition line is split by the second-order quadrupole perturbation.

The situation is described by the spin Hamiltonian

$$\mathcal{H} = -\hbar\nu_L(1 + K_{zz'})I_z' + \frac{\hbar\nu_Q}{2}(3I_z'^2 - I_z'^2),$$

appropriate for tetragonal crystals. Here $z'$ is the direction of the applied field ($H_{\text{ext}}$) and $z$ is the direction of the principal axis of the EFG. $\nu_L = \gamma H_{\text{ext}}/2\pi$ is the Larmor frequency and $K_{zz'}$ represents the NMR shift. The quadrupole frequency for an $I = 3/2$ nucleus can be expressed as $\nu_Q = e^2 Q V_{zz'}/2\hbar$, $e$ is the electron charge, $Q$ is the nuclear quadrupole moment, $V_{zz'}$ is the EFG and $h$ is Planck’s constant. According to this Hamiltonian, the NMR spectrum depends on the angle $\theta$ between the external field and the EFG principal axis. To first order, the quadrupole satellite resonance frequencies are given by

$$\nu_{\pm} = \nu_L(1 + K_{zz'}) \pm \frac{\nu_Q}{2}(3\cos^2 \theta - 1)$$

In second order perturbation theory, the central transition frequency depends on $\theta$ according to

$$\nu(\theta) = \nu_L(1 + K_{zz'}) - \frac{3\nu_Q^2}{16\nu_L}\sin^2 \theta(9\cos^2 \theta - 1).$$

In a powder sample, crystallites with all values of $\theta$ are present. Under these conditions the quadrupole satellites appear as sharp peaks at $\nu_L(1 + K_{zz'}) \pm \nu_Q/2$ which correspond to $\theta = 90^\circ$. For a powder, sharp peaks are observed in the central transition for $\theta = 90^\circ$ and $\theta = \cos^{-1}(\sqrt{5}/9) = 41.8^\circ$, as shown by the calculated powder-pattern spectrum in Fig. 2. The calculated spectrum assumes no preferential orientation of crystal grains, which is reasonable because the solidifications of the pressure medium prevent the crystal grains from reorienting. In a field-swept spectrum, the $\theta = 90^\circ$ peak occurs at lower field, as indicated in Fig. 2. Since the EFG principal axis is along the $c$ direction in KFe$_2$As$_2$, the $\theta = 90^\circ$ peak arises from those crystallites that experience an external field in the crystal ab plane. We conducted our NMR shift and $1/T_1$ measurements at this peak of the central transition.

The quadrupole resonance frequency $\nu_Q$ was obtained by a direct measurement of the NQR spectrum at zero magnetic field. The typical NQR spectrum is shown in...
The central transition line is split into two lines by the second order quadrupole effect. $\theta$ is the angle between the external field and the principal axis of the electric field gradient (see text). The red curve is a simulated powder spectrum with $\nu_Q = 12.66$ MHz.

In order to precisely determine the NMR shift with external field applied in the $ab$ plane, we performed Fourier transform measurements of the $\theta = 90^\circ$ peak of the NMR central transition line at a constant magnetic field. In general, the central transition frequency is given by

$$
\nu(\theta) = \nu_L \left( 1 + \frac{2K_{ab} + K_c}{3} \right)
+ \frac{\nu_L}{3}(K_c - K_{ab})(3\cos^2\theta - 1)
- \frac{3\nu_Q^2}{16\nu_L}\sin^2\theta(9\cos^2\theta - 1).
$$

where $K_{ab}$ and $K_c$ are Knight shifts for $H \parallel ab$ plane and $H \parallel c$ axis, respectively. In the present case, since $3\nu_Q^2/16\nu_L \gg \nu_L(K_c - K_{ab})$ (Ref. 8 gives $|K_c - K_{ab}| \sim 0.001$), Eq. 6 can be simplified as

$$
\nu(\theta = 90^\circ) = \nu_L(1 + K_{ab}) + \frac{3\nu_Q^2}{16\nu_L}
$$

when $\theta = 90^\circ$. We therefore obtain $K_{ab}$ by subtracting $3\nu_Q^2/16\nu_L$ from the measured resonance frequency, $\nu(\theta = 90^\circ)$.

The obtained NMR shifts are shown in Fig. 3. At ambient pressure, the NMR shift is nearly constant at low temperature and shows a broad peak near 150 K, before decreasing at high temperature. The behavior of $K_{ab}$ is qualitatively similar under pressure, with the broad peak shifting to slightly higher temperature.

### C. Crossover temperature $T^*$

The NMR shift data in Fig. 4 are consistent with a coherence/incoherence crossover behavior in KFe$_2$As$_2$ at all measured pressures. The broad peak in the NMR spectrum of KFe$_2$As$_2$ powder measured at $T = 10$ K and $p = 1.9$ GPa.

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FIG. 4: NMR shift with external field aligned in the \(ab\) plane \(\left(K_{\text{ab}}\right)\) for indicated pressures. The dashed lines are guides to the eye. The arrows represent the crossover temperature \(T^*\) as determined by NMR \(1/T_1\) measurements (see text and Fig. 5). The horizontal bars denote the uncertainty in estimation of \(T^*_\text{NMR}\) (\(\pm 20\) K).

shift has been interpreted as the crossover from the high-temperature local-moment (Curie Weiss) behavior to the low temperature coherent state \(6, 28\). We could not reliably extract the crossover temperature \(T^*\) from the NMR shift data alone because of the weak temperature dependence of the NMR shift and also the broad quadrupole powder lineshape, although the data suggest a small increase of \(T^*\) under pressure.

The coherence/incoherence crossover temperature in \(\text{KFe}_2\text{As}_2\) can also be estimated from the nuclear spin-lattice relaxation rate \(1/T_1\) data, shown in Fig. 5. Our results for \(1/T_1\) at ambient pressure are quantitatively consistent with Ref. \(8\). At low temperature, \(1/T_1\) shows a power law behavior \(1/T_1 \sim T^{0.75}\) for all pressures, as seen in Fig. 5. An obvious reduction in the slope of \(1/T_1\) is seen at high temperature, however. Similar temperature dependence of \(1/T_1\) is often observed in heavy fermion systems, where \(1/T_1\) shows a power law behavior of \(1/T_1 \propto T^{\alpha}\) (i.e. \(\alpha = 0.25\) in \(\text{CeCoIn}_5\) \(49\) and \(\alpha = 1\) in \(\text{URu}_2\text{Si}_2\) \(50\)) at low temperatures due to coherent metallic heavy fermion states and levels off at higher temperatures due to incoherent local moment behaviors. Thus the change in slope of the temperature dependence of \(1/T_1\) gives an estimate of the coherence/incoherence crossover temperature (defined as \(T^*_\text{NMR}\)). From the \(T_1\) data, we find \(T^*_\text{NMR} \sim 145 \pm 20\) K at ambient pressure, \(T^*_\text{NMR} \sim 170 \pm 20\) K at 1.5 GPa and \(T^*_\text{NMR} \sim 180 \pm 20\) K at 2.1 GPa, indicating that \(T^*_\text{NMR}\) increases under pressure. The uncertainty in \(T^*_\text{NMR}\) is due primarily to uncertainty in the high-\(T\) slope (see below). These values of \(T^*_\text{NMR}\) seem to be consistent with the high-temperature end of the broad peak of \(K_{\text{ab}}\) (arrows in Fig. 4). The increase of \(T^*_\text{NMR}\) under pressure is reasonable, as the application of pressure should increase the hybridization between localized and itinerant electrons, thus increasing the local magnetic coupling \(J\) \(23\).

We also note that \(1/T_1\) constant behavior above the coherent/incoherent crossover temperature \(T^*\) is observed in \(\text{CsFe}_2\text{As}_2\) \(28\), which has the highest effective mass of the \(\text{AF}_2\text{As}_2\) \((A = \text{K}, \text{Rb}, \text{Cs})\) family and therefore most localized electrons. However, as seen in Fig. 4 in \(\text{KFe}_2\text{As}_2\) at ambient pressure \(1/T_1\) does not level off completely above \(T^*_\text{NMR}\) but rather increases much more slowly, following roughly \(1/T_1 \sim T^{0.25\pm 0.1}\). Furthermore, as \(T^*_\text{NMR}\) increases under pressure, so does the slope of \(1/T_1 \sim T^{0.4\pm 0.1}\). It would be interesting if the higher temperature slope correlates with extent of the localization.

To corroborate our estimate of \(T^*\) and expand the results to pressures higher that those attainable in our NMR pressure cell, we also present and re-analyze single-crystal resistivity data up to \(\sim 5\) GPa \(20\), as shown in Fig. 6(a). In heavy fermion systems, one expects a decrease of the resistivity below the coherence temper-
where the scaling coefficient $T^*$ is chosen so as to merge each curve with the ambient pressure curve. For ambient pressure, $T^* = 1$. Upper inset: pressure dependence of the unitless scaling factor $t^*$. Lower inset: Comparison of pressure dependence of $T^*$ as measured by resistivity ($T^*_{\text{R}}$; filled symbols) and NMR ($T^*_{\text{NMR}}$; open symbols). For resistivity $T^*_{\text{R}} = (157 K) t^*$, where $T^*_{\text{R}}$ at 0 GPa is determined by the crossing of two tangent lines, as proposed in Ref. 28 (see text).

This method, then, appears to give a reasonable estimate of $T^*$ in these materials. Here we also apply this method to estimate $T^*$ (defined as $T^*_{\text{R}}$) in KFe$_2$As$_2$ using the resistivity data. We note that our resistivity curves for different pressures can be scaled by a pressure dependent scaling factor $t^*$ (defined dimensionless), as shown in Fig. 6(b). The pressure dependence of $t^*$ is shown in the upper inset. To estimate $T^*_{\text{R}}$ from the resistivity data, we use the cross point of two approximately linear trends as shown in Fig. 6(b) where $T^*_{\text{R}}$ is estimated to be $T^*_{\text{R}} = 157 K$ for the ambient pressure data. Then, the pressure dependence of $T^*_{\text{R}}$ can be obtained by using the pressure dependence of $t^*$. As shown in the lower inset of Fig. 6(b), $T^*_{\text{R}}$ increases with increasing pressure. While the values of $T^*_{\text{R}}$ extracted from the resistivity data up to 2.1 GPa are slightly higher than the $T^*_{\text{NMR}}$ values identified by NMR data, both techniques show the increase of the coherent/incoherent crossover temperature $T^*$ with applied pressure. It is clear that $T^*_{\text{R}}$ evolves continuously, showing no anomaly at $p_c \approx 1.8$ GPa. It is interesting to note that the resistivity data for the Rb- and Cs-samples can also be scaled to our ambient pressure data with $t^* = 0.78 \ (T^*_R = 123 K)$ and $t^* = 0.52 \ (T^*_R = 82 K)$ respectively.

We now consider the empirical relation that $T_c$ is proportional to $T^*$ observed in the AFe$_2$As$_2$ (A = K, Rb, Cs) family at ambient pressure 28. Figure 7 plots our results for $T_c$ as a function of $T^*$ along with the results of Ref. 28. In the AFe$_2$As$_2$ (A = Cs, Rb, K) family at ambient pressure, $T_c$ moves in proportion to $T^*$, suggesting that the change of $T^*$ is the primary factor in determining $T_c$. In contrast, for pressurized KFe$_2$As$_2$ we find that $T_c$ decreases sharply as a function of $T^*$ below $p_c \approx 1.8$ GPa and then becomes roughly independent of $T^*$ above $p_c$. These results indicate that $T^*$ is not the primary driver of the pressure dependence of $T_c$ in KFe$_2$As$_2$. Instead, as will be described in the next section, we show the antiferromagnetic spin fluctuations play an important role for the pressure dependence of $T_c$.

Finally, it is interesting to discuss the second empirical relation that $\gamma^{-1} \propto T^*$ under pressure. Quantum oscillation experiments under high pressure found that the effective mass $m^*$ decreases under pressure 14. In addition, the coefficient $A$ in the low-temperature resistivity $\rho = \rho_0 + AT^2$ decreases smoothly, which is also consistent with a decreasing $m^*$ under pressure 29. The decreasing $m^* \sim \gamma$ accompanied by the increase of $T^*$ suggest that the $\gamma^{-1} \propto T^*$ relationship seems to hold under pressure, similar to the case of AFe$_2$As$_2$ (A = K, Rb, Cs). As one moves from CsFe$_2$As$_2$ to RbFe$_2$As$_2$ to KFe$_2$As$_2$, the chemical pressure increases due to the decreasing size of the alkali metal ion 8. Simultaneously, $T^*$ increases 28. Consequently, the increase of $T^*$ in KFe$_2$As$_2$ under physical pressure could be considered an extension of the chemical pressure trend. However, it is noted that the $\gamma^{-1} \propto T^*$ relationship does not appear to hold the case.
FIG. 8: NQR 1/T1 above Tc for various pressures. The solid red curve for ambient pressure is a power law fit (see text). Inset: The value of NQR 1/T1 at 4.2 K as a function of pressure.

D. NQR Spin-Lattice Relaxation Rate

Since T* evolves smoothly across the critical pressure p_c, the pressure dependence of the coherence/incoherence crossover behavior cannot explain the non-monotonic behavior of T_c under pressure in KFe_2As_2. To address this question, we have also performed NQR 1/T1 measure-
different behavior of \( T_c \) between the pressure and replacement cases is not understood well, we here discuss a few possibilities to explain the difference.

One possible difference between the pressure and replacement cases may relate to the anisotropy of magnetic fluctuations. According to Zhang et al. [52], based on their NMR data, the anisotropy of the low-temperature AFM fluctuations is found to significantly decrease with the replacement from Cs to K in AFe\(_2\)As\(_2\). That is, the Cs sample with the lowest \( T_c \) in the family has the greatest anisotropy, suggesting that \( T_c \) may correlate with the anisotropy of the AFM fluctuations. Zhang et al. also suggested that the difference of the anisotropy may relate to quantum criticality and that the Cs sample is the closest to a QCP.

It is interesting to compare this to the behavior of the magnetic fluctuation anisotropy in KFe\(_2\)As\(_2\) under pressure which can be obtained by taking a look at the ratio of \( 1/T_1 \) for the two field directions, \( R \equiv (1/T_1)_{ab}/(1/T_1)_c \). According to the previous NMR studies performed on Fe pnictide SCs [8, 53, 54], the ratio \( R \) depends on the nature of magnetic fluctuations and also anisotropy of the magnetic fluctuations as

\[
R = \begin{cases} 
0.5 + \frac{(S_{ab})^2}{S_c} & \text{for the stripe AFM fluctuations} \\
0.5 & \text{for the Néel-type spin fluctuations}
\end{cases} \tag{9}
\]

where \( S_\alpha \) is the amplitude of the spin fluctuation spectral density at NMR frequency along the \( \alpha \) direction. Unfortunately, since we used a powder sample to improve the signal intensity, only \( H||ab \) plane \( 1/T_1 \) NMR measurements are feasible. Nevertheless, we can obtain some information about the anisotropy of the AFM spin fluctuations using our NQR \( 1/T_1 \) data. Since the quantization axis of the electric field gradient is parallel to the \( c \) axis, the NQR \( 1/T_1 \) should reflect magnetic fluctuations perpendicular to the \( c \) axis. These are the same fluctuations observed by NMR \( 1/T_1 \) for \( H||c \) axis, where the quantization axis is determined by the magnetic field. Indeed, we confirmed that our NQR \( 1/T_1 \) data coincide almost perfectly with the NMR \( 1/T_1 \) data under \( H||c \) axis reported previously at ambient pressure [8], as shown in the inset of Fig. 9. This also indicates no magnetic field effects on \( 1/T_1 \). Therefore, using both the NQR \( 1/T_1 \) and NMR \( 1/T_1 \) data under pressure, we can estimate how the anisotropy of magnetic fluctuations changes with pressure. The estimated \( R \) values using both the NQR \( 1/T_1 \) and NMR \( 1/T_1 \) data are shown in Fig. 9 as a function of temperature for different pressures. All \( R \) values are greater than unity, consistent with the stripe-type spin fluctuations. As shown, \( R \) does not show any significant change with pressure. This indicates that the anisotropy of spin fluctuations is almost independent of pressure, in contrast to the case of replacement effects on AFe\(_2\)As\(_2\).

We suggest that the different behaviors of the spin fluctuation anisotropy between the pressure and replacement cases may be related to the different behavior of \( T_c \) in the two cases. It is also interesting to note that several papers have proposed that, in the proximity of a QCP, the critical fluctuations may actually be detrimental to superconductivity in these systems [6, 26, 52]. Since CsFe\(_2\)As\(_2\) is considered to be the closest to the QCP, it would be expected to have a low \( T_c \).

It is also interesting to note in this context that in the hole-overdoped region of the \( Ba_{1-x}K_xFe_2As_2 \) phase diagram, the AFM spin fluctuations and Sommerfeld coefficient determined by specific heat measurements are both enhanced with increasing \( x \) while \( T_c \) decreases, similar to the case of AFe\(_2\)As\(_2\) (\( A = K, Rb, Cs \)). One possible explanation for the decrease of \( T_c \) in \( Ba_{1-x}K_xFe_2As_2 \) is the growth of competing ferromagnetic (FM) spin fluctuations, which coexist with the AFM spin fluctuations [9]. As demonstrated by Wiecki et al., the growth of the AFM fluctuations with increasing \( x \) in \( Ba_{1-x}K_xFe_2As_2 \) is accompanied by the simultaneous growth of FM fluctuations. These FM fluctuations may interfere with the AFM-fluctuation-based Cooper-pairing mechanism, thus lowering \( T_c \) despite the enhancement of AFM fluctuations. It is possible such physics could apply to the AFe\(_2\)As\(_2\) (\( A = K, Rb, Cs \)) system also.

2. Superconducting State

The \( T \) dependence of NQR \( 1/T_1 \) below \( T_c \) is shown in Fig. 10. At ambient pressure, \( 1/T_1 \) follows the power law \( 1/T_1 \sim T^{0.8} \) in the PM state as discussed above (red dashed line in Fig. 10). A clear kink is seen at \( T_c \), and
Then, we fit the recovery curves according to

\[ 1 - \frac{m(t)}{m(\infty)} = A \exp(-3t/T_{1S}) + (1-A) \exp(-3t/T_{1L}), \]

where \( T_{1S} \) and \( T_{1L} \) are the short and long relaxation times, respectively. The parameter \( A \), representing the fraction of nuclei relaxing with the shorter relaxation time \( T_{1S} \), is shown in the lower inset of Fig. 10 demonstrating that the long \( T_{1L} \) component fraction increases with decreasing temperature.

The existence of two \( T_1 \) components implies the existence of two distinct local electronic environments, which are physically separated in real space. Similar two-component relaxation has been observed by NQR in the closely-related sample RbFe\(_2\)As\(_2\), in which the two-component behavior was argued to be associated with a charge order of nanoscale periodicity \[27\]. While we find no direct evidence for charge order in KFe\(_2\)As\(_2\) in this study, charge ordering in KFe\(_2\)As\(_2\) at 2.4 GPa (above our maximum pressure) was proposed by high pressure NMR \[9\]. Two-component relaxation has also been reported in CsFe\(_2\)As\(_2\) under magnetic field in Refs. 28 (Supplemental Information), 29 and 30. At present, although the origin of the two \( T_1 \) components in KFe\(_2\)As\(_2\) is not clear, the similar behavior in closely related systems would suggest that the two-component behavior observed here is intrinsic. Further studies will be needed to clarify the origin.

NQR \( 1/T_1 \) is a sensitive probe of the reduction of the density of states (DOS) at the Fermi energy \( N(E_F) \) due to the opening of the SC gap. In general, \( 1/T_1 \) in the SC state is given by \[56\]

\[ \frac{1}{T_1} \sim \int_0^\infty \left[ N_s^2(E) + M_s^2(E) \right] f(E)(1-f(E))dE, \]  \( \text{(11)} \)

where \( N_s(E) \) is the DOS and \( f(E) \) is the Fermi distribution function. \( M_s(E) \) is the anomalous DOS arising from Cooper pair coherence. Due to the lack of a coherence peak just below \( T_c \), we neglect the coherence term, as has been done in previous NMR/NQR studies of Fe\(_{2}\)As superconductors.

The very weak decrease of the short component \( 1/T_{1S} \) below \( T_c \) \( (1/T_{1S} \sim T^{-1.3}) \), implies a very small SC gap. Using a simple full gap model for \( N_s(E) \), we estimate a gap of \( \Delta(0) \sim 0.07 \text{ meV} \) \( (2\Delta(0)/k_B T_c \sim 0.5) \) from the short component, consistent with \( 2\Delta(0)/k_B T_c \sim 0.51 \) reported by previous NQR measurements \[11\]. For all but the lowest temperatures measured, the relaxation is dominated by the short component, as shown by the inset of Fig. 10. This implies that a large number fraction of nuclei see a nearly gapless electronic environment below \( T_c \).

The data follow a new power law \( 1/T_1 \sim T^{-1.3} \) below \( T_c \) (red solid line in Fig. 10). This behavior is consistent with previous ambient pressure NQR results \[11\]. However, in contrast to Ref. \[11\], a long \( T_1 \) component is found to appear below \( T = 1 \text{ K} \) at ambient pressure and also under pressure. The upper inset of Fig. 10 shows the typical two-component exponential behavior of the nuclear magnetization recovery curve observed at low temperature \( (T = 0.4 \text{ K}; p = 1.5 \text{ GPa}) \), together with a single exponential behavior at \( T = 3.73 \text{ K} \) and \( p = 1.5 \text{ GPa} \). Then, we fit the recovery curves according to

\[ 1 - \frac{m(t)}{m(\infty)} = A \exp(-3t/T_{1S}) + (1-A) \exp(-3t/T_{1L}). \]

\( \text{(10)} \)
walls inherent to antiferromagnetism in iron pnictide SCs.

In contrast, the long component $1/T_{1L}$ shows a large reduction relative to the $1/T_1$ in the PM state, implying a large reduction in $N_s(E_F)$ due to the SC gap. Although the experimental uncertainty is large, $1/T_{1L}$ seems to be proportional to $T^{2\pm1}$ as shown by the solid line in Fig. 10. The sizable depletion of $N_s(E_F)$ only below $T \sim 1$ K has been observed by the STS and ARPES experiments. The co-existence of one large gap and at least one very small gap has also been reported with specific heat and small angle neutron scattering experiments. However, from the two-component relaxation behavior, our NQR data suggest a real-space modulation of the local gap structure, which has not been reported previously.

Under high pressure of 1.5 GPa and above, no obvious change of the slope of the short $T_1$ component occurs across $T_c$ within our experimental uncertainty. This indicates that the nuclei relaxing according to $1/T_1$ see a gapless local electronic environment above 1.5 GPa. Therefore the small gap seen by $1/T_{1S}$ at ambient pressure is thought to be suppressed to zero near $p_c$, and is not recovered above $p_c$. Similarly, muon spin rotation ($\mu$SR) measurements on the closely-related RbFe$_2$As$_2$ with $p_c \sim 1.1$ GPa reported that the smaller of two SC gaps is suppressed to zero near 1 GPa. As for the long $T_1$ component under high pressure, as shown in Fig. 10, no obvious change in $1/T_{1L}$ can be found, suggesting no dramatic change in the magnitude of the larger SC gap upon pressure application. According to Ref. 24, the SC gap structure changes above $p_c$, where the SC gap is modulated along $k_z$. However, we did not observe a clear change in gap symmetry across $p_c$ from our $1/T_1$ measurements.

IV. CONCLUSIONS

We have presented $^{75}$As-NMR, NQR and resistivity data which clearly show an increase of the coherence/incoherence crossover temperature $T^*$ in KFe$_2$As$_2$ under pressure. This increase of $T^*$ is expected due to the increase in hybridization between localized and conducting bands caused by pressure application. We find that the relation $\gamma^{-1} \sim T^*$ observed in ambient pressure AFe$_2$As$_2$ (A = K, Rb, Cs) continues to hold under pressure. However, the proportionality between $T^*$ and $T_c$ is clearly broken under pressure. The non-monotonic behavior of $T_c$ under pressure is therefore unrelated to the coherence-incoherence crossover behavior in the paramagnetic state. However, the strength of AFM spin fluctuations in the paramagnetic state is found to correlate with $T_c$, evidencing clearly that the AFM spin fluctuations play an important role for the appearance of superconductivity in KFe$_2$As$_2$, although such a correlation cannot be seen in the replacement effects of A in the AFe$_2$As$_2$ (A = K, Rb, Cs) family. In the superconducting state, two $T_1$ components are observed at low temperatures, suggesting the existence of two distinct local electronic environments. The temperature dependence of the short $T_{1s}$ indicates nearly gapless state below $T_c$. On the other hand, the temperature dependence of the long component $1/T_{1L}$ implies a large reduction in the density of states at the Fermi level due to the SC gap formation. These results suggest a real-space modulation of the local SC gap structure in KFe$_2$As$_2$ under pressure.

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