Magnetic quantum ratchet effect in (Cd,Mn)Te- and CdTe-based quantum well structures with a lateral asymmetric superlattice

P. Faltermeier, G.V. Budkin, J. Unverzagt, S. Hubmann, A. Pfaller, V.V. Bel’kov, L.E. Golub, E.L. Ivchenko, Z. Adamus, G. Karczewski, T. Wojtowicz, V.V. Popov, D.V. Fateev, D.A. Kozlov, D. Weiss, and S.D. Ganichev

1 Terahertz Center, University of Regensburg, 93040 Regensburg, Germany
2 Ioffe Institute, 194021 St. Petersburg, Russia
3 Institute of Physics, Polish Academy of Sciences, al. Lotników 32/46, PL 02-668 Warszawa, Poland
4 International Research Centre MagTop, al. Lotników 32/46, PL 02-668 Warszawa, Poland
5 Institute of Radio Engineering and Electronics (Saratov Branch), 410019 Saratov, Russia
6 Saratov State University, 410012 Saratov, Russia and
7 A.V. Rzhanov Institute of Semiconductor Physics, 630090 Novosibirsk, Russia

We report on the observation of magnetic quantum ratchet effect in (Cd,Mn)Te- and CdTe-based quantum well structures with an asymmetric lateral dual grating gate superlattice subjected to an external magnetic field applied normal to the quantum well plane. A dc electric current excited by cw terahertz laser radiation shows 1/B-oscillations with an amplitude much larger as compared to the photocurrent at zero magnetic field. We show that the photocurrent is caused by the combined action of a spatially periodic in-plane potential and the spatially modulated radiation due to the near field effects of light diffraction. Magnitude and direction of the photocurrent are determined by the degree of the lateral asymmetry controlled by the variation of voltages applied to the individual gates. The observed magneto-oscillations with enhanced photocurrent amplitude result from Landau quantization and, for (Cd,Mn)Te at low temperatures, from the exchange enhanced Zeeman splitting in diluted magnetic heterostructures. Theoretical analysis, considering the magnetic quantum ratchet effect in the framework of semiclassical approach, describes quite well the experimental results.

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I. INTRODUCTION

Spatially periodic non-centrosymmetric systems are able to transport nonequilibrium particles in the absence of an average macroscopic force resulting in the ratchet effect [1–5]. Ratchet effects whose prerequisites are simultaneous breaking of both thermal equilibrium and spatial inversion symmetry can be realized in a great variety of forms and in particular, as electric transport in semiconductor systems [6–20]. Recent experiments demonstrated that terahertz radiation induced ratchet effects, can be efficiently excited in semiconductor quantum wells (QW) [14, 15, 21, 22] and graphene [23, 24] with lateral superlattice structures. These experiments allowed one to explore basic physics of the ratchet effects in low dimensional electron systems, provide information on nonequilibrium transport in such systems and demonstrate that ratchet effects can be applied for room temperature terahertz radiation detection [25–28]. The latter, besides high sensitivity and short response times, offer new functionality being a good candidate for all-electric detection of the radiation polarization state including radiation helicity [29–32].

Here we report on the observation and study of magnetic quantum ratchet effect in (Cd,Mn)Te/(Cd,Mg)Te diluted magnetic heterostructures and CdTe/CdMgTe QWs superimposed with lateral asymmetric superlattices. Applying magnetic field \( B \) along the growth direction we observe that the ratchet current exhibits sign-alternating 1/B-periodic oscillations with amplitudes immensely larger than the ratchet signal at zero magnetic field. The results are analyzed in terms of the theory of magnetic ratchet effects in QW structures with a lateral asymmetric periodic potential [33]. We show that the photocurrent generation is based on the combined action of a spatially periodic in-plane potential and the spatially modulated light due to the near field effects of radiation diffraction. Corresponding theoretical analysis describes the experimental results.

The paper is organized as follows. First, we present our samples and results of magneto-transport characterization (Sec. II), as well as briefly describe the experimental technique (Sec. III). In Sec. IV we discuss the results on the photocurrents generated at zero magnetic field. Section V contains the main experimental results on the magnetic quantum ratchet effect. It has three subsections describing the basic results, the laser beam scan across the structure and the effect of the electrostatic potential acting on the electron gas. In the following Sec. VI we present the theory, calculate dependencies of the photocurrent on magnetic field, and compare them with the experimental data. Finally, in Sec. VII, we summarize the results and discuss perspectives of future experimental studies of the magnetic quantum ratchet effect.
well resolved quantum Hall plateaux have been observed. Two characteristic dependencies measured in Hall bar and van-der-Pauw geometries in (Cd,Mn)Te structures are shown in Figs. 2(a) and 2(b), respectively. While the amplitude of the oscillations increases in CdTe and (Cd,Mn)Te structures at rather high temperatures with raising magnetic field, the amplitude of the oscillations in (Cd,Mn)Te at low temperatures is a more complex function of the magnetic field $B$ and shows a beating like pattern. The latter is clearly seen in Fig. 2(a) for $T = 1.6 \text{ K}$ ($B > 3.5 \text{ T}$) and in panel (b) for $4.2 \text{ K}$ ($B > 4.5 \text{ T}$). Such a behavior in diluted magnetic semiconductor (DMS) structures is well known to be caused by the exchange interaction of electrons with Mn$^{2+}$ ions resulting in the exchange-enhanced Zeeman splitting [39, 41–43].

FIG. 1: (a) Sketch of CdMgTe/(Cd,Mn)Te/CdMgTe QW. Two red bars show evenly spaced three-monolayer-thick Cd$_{0.8}$Mn$_{0.2}$Te layers inserted during QW growth. (b) Cross-section of the dual-grating gate superlattice formed by metal fingers deposited on top of the QW structure. Structure composition is given on the right side of the sketch. The supercell of the grating gate fingers consists of metal stripes having two different widths $d_1$ and $d_2$ separated by spacings $a_1$ and $a_2$. This asymmetric supercell is repeated $N$ times to create a superlattice with period $d = d_1 + a_1 + d_2 + a_2$, see Table I. (c) Photograph of the sample together with schematic top view of the dual-grating gate superlattice. Thin red and thick blue lines sketch the top gates having different thicknesses and spacings.

B. Dual grating top gate structure

For the ratchet effect experiments we fabricated a dual grating top gate (DGG) superlattices on top of the QW structures. A sketch of the gate fingers and a corresponding optical micrograph are shown in Figs. 1(b) and 1(c), respectively.

II. SAMPLES

A. Samples grow and characterization

Experiments are carried out on (Cd,Mn)Te/CdMgTe and CdTe/CdMgTe single QW structures grown by molecular beam epitaxy on (001)-oriented GaAs substrates [34–38]. During the growth the fluxes of Cd, Te, Mg and Mn have been supplied from elemental sources while Iodine flux has been obtained from a ZnI$_2$ source. The schematic layout of the (Cd,Mn)Te/CdMgTe layer structure and sketch of the QW are presented in Fig. 1. The thick buffer (≈ 6 µm), consisting of CdTe and Cd$_{0.76}$Mg$_{0.24}$Te layers and CdTe/Cd$_{0.76}$Mg$_{0.24}$Te short period superlattices, have been grown to reduce the number of dislocations resulting from the strong lattice mismatch between GaAs and Cd$_{1-x}$Mg$_x$Te. The well width in both kinds of structures is 9.7 nm and the Cd$_{0.76}$Mg$_{0.24}$Te alloy serves as a barrier material. The composition of barriers has been determined from photoluminescence spectra. In order to obtain a two-dimensional electron gas the structures have been modulation doped by Iodine donors incorporated into the 5 nm thick region of the top barrier at the distance of either 10 or 15 nm away from the QW, in (Cd,Mn)Te/CdMgTe and CdTe/CdMgTe structures, respectively. Doped regions have been overgrown by an undoped cap layer with thickness of either 50 nm, for (Cd,Mn)Te/CdMgTe QWs, or 75 nm, for CdTe/CdMgTe QWs. The density of the two-dimensional electron gas, $n_e$, and the electron mobility, $\mu$, determined at liquid helium temperature (4.2 K) for (Cd,Mn)Te/CdMgTe structures are $n_e = 6.6 \times 10^{11}$ cm$^{-2}$ and $\mu = 9.5 \times 10^{3}$ cm$^2$/Vs, and for CdTe/CdMgTe structures $n_e = 4.2 \times 10^{11}$ cm$^{-2}$ and $\mu = 65 \times 10^{3}$ cm$^2$/Vs.

(Cd,Mn)Te/CdMgTe structures contain a single QW made of (Cd,Mn)Te digital magnetic alloy [39], while CdTe/CdMgTe structures contain a single QW made of non-magnetic CdTe. In the former structures two evenly spaced Cd$_{0.8}$Mn$_{0.2}$Te thin layers were inserted during the QW growth, see Fig. 1(a). These two layers were three-monolayer-thick (ML) and separated from each other and from the barriers by 8 ML thick CdTe (1 ML is 0.324 nm thick).

Incorporation of Mn$^{2+}$ ions carrying localized spin $S = 5/2$ into the QW region leads to a strong enhancement of the effective $g$ factor of band carriers, and hence to an enhanced Zeeman splitting. This has been shown in previous magneto-photoluminescence (PL) studies performed on the (Cd,Mn)Te/CdMgTe samples made from the same wafer as used in the current study. Magneto-PL showed strong red-shift of the PL line with increasing magnetic field [37]. From fitting of the modified Brillouin function [40, 41] to the field dependence of the PL line position the effective average concentration of Mn in the digital alloy has been estimated to be $\bar{x} = 0.015$.

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| Sample | #1 | #2 | #3 | #4 | #5 | #6 |
|--------|----|----|----|----|----|----|
| material | CdMnTe | CdMnTe | CdMnTe | CdTe | CdTe | CdTe |
| Au | 25 nm | 30 nm | 15 nm | 25 nm | 25 nm |
| Dy | - | - | 75 nm | - | - |
| $d_1$ ($\mu$m) | 1.85 | 1.7 | 1.7 | 1.7 | 1.85 |
| $a_1$ ($\mu$m) | 2.8 | 3.5 | 2.8 | 2.8 | 2.8 |
| $d_2$ ($\mu$m) | 3.7 | 3.7 | 3.7 | 3.7 | 3.7 |
| $a_2$ ($\mu$m) | 5.6 | 7 | 5.8 | 5.8 | 5.6 |
| $d$ ($\mu$m) | 13.95 | 15.9 | 14 | 14 | 13.95 |
| $l$ ($\mu$m) | 905 | 880 | 875 | 875 | 905 |
| $N$ | 65 | 56 | 63 | 63 | 65 |
| $w_1$ ($\mu$m) | 600 | 450 | 450 | 450 | 600 |
| $w_2$ ($\mu$m) | 200 | 350 | 350 | 350 | 200 |

TABLE I: Sample parameters shown in detail in Figs. 1(b) and 1(c).

The grating-gate superlattice consists of two metal stripes having widths $d_1$ and $d_2$ and spacings $a_1$ and $a_2$. The widths of the thin stripes were either $d_1 = 1.7$ or 1.85 $\mu$m, that of the wide stripes $d_2 = 3.7$ $\mu$m, see Tab. I. Spacings in most of the structures were $a_1 = 2.8 \mu$m and $a_2 = 5.6 \mu$m. To clarify the influence of the superlattice parameters on the ratchet effect, we additionally fabricated one DGG structure with substantially different spacings $a_1 = 3.5 \mu$m and $a_2 = 7.0 \mu$m between the stripes. The superlattice is repeated $N$ times to produce an asymmetric superlattice with the period $d = d_1 + a_1 + d_2 + a_2$, see Refs. [21, 23, 44]. The two sub-grating gates, each formed by stripes of identical width, can be biased independently. For this purpose all thin (top gate G1) and thick (top gate G2) grating stripes have been connected by additional gold stripes, see thick horizontal lines in Fig. 1(c). The benefit of this geometry is that the periodic lateral electrostatic potential of the DGG structure can be varied in a controllable way. Several $4 \times 10$ and $4 \times 4 \text{mm}^2$ size samples of the same batch were prepared. The DGG structure has been fabricated on one half of the samples so that the other half of the sample surface remains unpatterned serving as reference part. It has a total area of $w_2 \times Nd$ where $w_2$ is the overlap length of two gate lattices being of the order of hundreds of micrometer.

In all samples, besides the sample #4, the gate fingers have been made by electron beam lithography and subsequent deposition of 25 or 30 nm thick gold films. The DGG structure of sample #4 has been fabricated by depositing 75 nm thick Dy and 15 nm thick Au films. Pre-magnetizing the hard magnetic Dy-based superlattice enables realization of a magnetic ratchet which features an inhomogeneous magnetic field, recently suggested in [33, 45].

For the photocurrent and magneto-transport measurements several pairs of ohmic contacts have been prepared, see inset in Figs. 2(b) and 3. Contact pads were placed in a way that the photo-induced currents can be measured perpendicularly to the metal fingers ($J_{x},$ contacts 1 and 4) and parallel to them ($J_{y},$ contacts 3 and 5). Two additional contacts (2 and 6) were used for detecting the photocurrent signals from the unpatterned area as a reference. Magneto-transport data for the (Cd,Mn)Te DGG structure at liquid helium temperature are shown in Fig. 2(b). Note that the application of gate voltages to individual gates does not visibly influence the period of $1/B$-oscillations of the longitudinal resistance, $R_{xx}$ (not shown). This is due to the fact that the area of DGG fingers is a very small fraction of the whole sample area. Moreover, the variation of bias voltage applied to gate 1 ($U_{G1}$) also does not substantially affect the value of $R_{xx}$ at a fixed magnetic field. The only detected deviation from the value of $R_{xx}$ at zero gate voltages is an increase of the resistance by $\sim 10\%$ for $U_{G2} \approx -0.35 \text{ V}$. The gate voltage dependencies of the longitudinal resistance measured at one of the maxima of the $R_{xx}$ oscillations are shown in the inset in Fig. 2(b). The dependencies are obtained at fixed magnetic field by sweeping the potential applied to one gate and holding the other one at zero bias. The observed behavior of $R_{xx}$ will be addressed below in the discussion of photocurrent data. Note that while the overall characteristic of the data obtained at different cooldowns is the same the onset of the resistance increase can be shifted on the gate voltage scale by $\pm 0.1 \text{ V}$. This is ascribed to cooldown dependent charge trapping in the insulator.
III. EXPERIMENTAL TECHNIQUE

For THz excitation we applied a continuous wave (cw) molecular optically pumped laser [46, 47]. The laser operated at the frequency \( f = 2.54 \) THz (photon energy \( h\omega = 10.4 \) meV, wavelength \( \lambda = 118 \) \( \mu \)m). The incident power about \( 30 \) mW was modulated at about 75 or 625 Hz by an optical chopper. The radiation at normal incidence was focused onto a spot of about 1.3 mm diameter. The spatial beam distribution had an almost Gaussian profile, measured by a pyroelectric camera [48]. Taking into account the size of the superlattice we obtain that the power irradiating the structure is \( P \approx 4 \) mW. The radiation intensity and electric field strength on the sample are \( I \approx 300 \) mW/cm\(^2\) and \( E_0 \approx 5.7 \) V/cm, respectively. Note that almost all experimental data, except the scan of the beam across the sample, are obtained for radiation focused on the DGG superlattice.

The structures were placed in a temperature variable optical magneto-cryostat. The photocurrents were studied in the temperature range between 2 and 9 K. The laser radiation was linearly polarized along the \( x \)-axis.

The photoresponse is measured by the voltage drop \( U \) across a load resistor \( R_L = 50 \) Ohm \( \ll R_s \) using standard lock-in technique. Here \( R_s \) is the sample resistance. The benefit of using of the small value of \( R_L \) is that the detected signal is unaffected by the sample resistance variation and is just proportional to the electric current generated by the THz radiation. The current is calculated via \( J = U/R_L \).

IV. PHOTOCURRENT AT ZERO MAGNETIC FIELD

We begin with briefly introducing the results obtained at zero magnetic field. While the paper is devoted to the observation of magneto-ratchet effect these results are important for further analysis of the data on magnetic field induced photocurrents.

Illuminating the DGG superlattice at normal incidence we have observed a photocurrent, whose magnitude and direction are sensitive to the electrostatic potentials applied to the first (G1) and the second (G2) gate sublattices. The photoresponse is detected perpendicularly to the gate stripes as well as along them. The fact that the photoresponse is generated by normally incident radiation provides a first indication that it is formed due to the presence of the superlattice. Indeed it is well known that in unpatterned (001)-oriented QW structures a photocurrent signal is only detectable under oblique incidence [37, 38]. The photocurrent consists of a contribution independent of the radiation polarization and a substantially smaller one dependent on the orientation of electric field vector \( E_0 \) of the linearly polarized radiation in respect to the orientation of the gate stripes. This has been demonstrated by measuring the photocurrent as a function the orientation of the \( E \)-field vector in respect to the \( x \)-axis (not shown). The same polarization behavior has been previously observed for the ratchet effect in lateral GaAs-based structures [14, 21] as well as in DGG structures fabricated on top of InAlAs/InGnAs/InAlAs/InP high electron mobility transistors (HEMT) [29] and graphene [23].

For unbiased gates, a non-zero built-in electrostatic potential is formed due to the presence of metal stripes in the QW vicinity. A direct evidence for the ratchet effect comes from the variation of the photocurrent by application of the bias voltages to the individual gates. Indeed the ratchet effect is known to be proportional to the averaged product

\[
\Xi = \frac{dV}{dx}|E(x)|^2
\]  

of the derivative of the coordinate dependent electrostatic potential \( V(x) \) and the distribution of the electric near-field \( E(x) \) [15–17, 20]. In the following, we call the parameter \( \Xi \) the lateral asymmetry. The value of \( \Xi \) may change sign depending on \( V(x) \). Consequently a variation of individual gate voltages should result in a change of the ratchet current including reversal of its direction, see the discussion in Sec. VI.

Exactly this behavior has been observed in the experiment. In order to tune the lateral asymmetry, we applied

![FIG. 3: Dependencies of the normalized magnitude \( J_{\parallel}/P \) on the gate voltage \( U_{G1} (U_{G2}) \) applied to the stripes at zero potential of the other gate \( U_{G2} = 0 (U_{G1} = 0) \). The polarization independent photocurrent contribution \( J_{\perp}^{\parallel} \) is extracted from the photocurrent polarization dependencies (not shown). The data are obtained for (Cd,Mn)Te QW sample #1 at zero magnetic field. Here and in the further plots, except for the one showing results on scan across the sample, the data are presented for the laser beam focused on the DGG superlattice. Insets show experimental geometries. Here and in the further plots, the data are obtained for linearly polarized radiation with the electric field vector \( E_0 \parallel x \) directed perpendicularly to the metal gate fingers.](image-url)
different bias voltages $U_{G1} \neq U_{G2}$ to the grating gates. Figure 3 demonstrates the influence of the gate voltage variation on the amplitude and sign of the polarization independent photocurrent $J^D$ [49]. Holding one of the gates at zero bias and varying the gate voltage on the other one we could controllably change the lateral asymmetry. The figure reveals that inversion of this lateral asymmetry obtained either by change of polarity of voltage applied to one gate or by interchange of gate voltage polarities applied to narrow and wide gates results in a change of sign of the photocurrent. This observation agrees well with the signature of ratchet currents: $J_x \propto \Xi$. Note that, while the overall characteristics of the data obtained at different cooldowns is the same, the photocurrent sign inversions can be shifted on the gate voltage scale by $\pm 0.1$ V. Similarly to the results addressed in Sec. II B this is ascribed to cooldown dependent charge trapping in the insulator. We also note that for large negative gate voltages all contributions vanish, which can be attributed to closing the transistor channel beneath the metal stripes of the DGG superlattice. Figure 3 also reveals that at large positive gate voltages the photocurrent saturates due to the effect of high electron densities.

To summarize, experiments at zero magnetic field provide a consistent picture demonstrating that the photocurrents are caused by the ratchet effect. They are (i) generated due to the lateral asymmetry, (ii) characterized by specific polarization dependencies for directions along and across the metal stripes, and (iii) change the direction upon reversal of the lateral asymmetry. These results are in full agreement with the theory of ratchet effects excited by the polarized THz electric field in asymmetric lateral superlattices, discussed below in Sec. VI. The overall behavior of the photocurrent is also in qualitative agreement with that of the electronic ratchet effects observed in semiconductor QW structures and graphene with a lateral superlattice [14, 15, 21, 23].

V. MAGNETIC FIELD INDUCED PHOTOCURRENT

A. Basic results

Now we turn to the main part of the paper devoted to magnetic field induced ratchet effects. Figure 4 shows the normalized photocurrent excited by linearly polarized radiation as a function of magnetic field applied perpendicularly to the QW plane. The principal observation is that with raising magnetic field the photocurrent drastically increases and, at high magnetic fields, exhibits sign-alternating 1/2-periodic oscillations. Moreover, Fig. 4 demonstrates that the reversal of the lateral asymmetry results in an inversion of the magneto-photocurrent direction providing a first clear indication that it is driven by the ratchet effect. Measurements of the magneto-photocurrent as a function of radiation power show that it scales linearly with the radiation power, i.e. quadratically with the radiation electric field, $E_0$, see inset in Fig. 5. Note that the positions of oscillation maxima/minima are independent of the radiation power, Fig. 5. Similar results, particularly magnetooscillations with current amplitudes much larger than the photocurrent at $B = 0$, are obtained for all studied samples. Studying various samples at different experimental conditions we found that the current in the $y$-direction is much smaller than $J_x$.

Data from the (Cd,Mn)Te QW sample #4 with ferromagnetic Dy gate are shown in Fig. 6. The period and magnitude of the 1/B-oscillations correlate with transport behavior and are very close to those shown for (Cd,Mn)Te QW samples with gold DGG structure presented for sample #1, Fig. 4.

Figure 7 shows another example of magneto-photocurrent measured for nonmagnetic CdTe QW sample #5 with gold DGG. While oscillations are clearly detected the signal is superimposed with a substantial background current. Because of the background the photocurrent, in contrast to samples #1 and #4, doesn’t change sign with varying magnetic field. The background photocurrent has also been obtained for (Cd,Mn)Te QW samples #2 and #3. We attribute an appearance of the background to imperfections of our large-size superlattices which are present in some structures as confirmed by optical microscope images [50]. The imperfections locally reduce symmetry and give rise to ratchet unrelated magneto-gyrotrophic photogalvanic currents in the “bulk” of the QW, see e.g. Ref. [51].
FIG. 5: Magnetic field dependencies of the photocurrent \( J_x \) measured at different levels of power ranging from 0.8 to 4.3 mW in (Cd,Mn)Te QW sample #1. Inset shows radiation power dependence of the photocurrent amplitude \( |J_x| \) for \( B = 3.9 \) T. Solid line is a linear fit.

B. Laser beam scan across the DGG structure

To prove that the magneto-ratchet effect stems from the irradiation of the superlattice we scanned the laser spot across the sample along the \( x \)-direction. The photocurrent \( J_x \) was measured for \( B = 4.39 \) T and the gate voltage combination \( U_{G1}/U_{G2} = 0/−0.5 \) V, i.e. at a maximum of one of the magneto-oscillations, Fig. 4. The photocurrent generated by linearly polarized radiation with \( E_0 \parallel x \) as a function of the radiation spot position and the corresponding experimental geometry are shown in Fig. 8. The photocurrent reaches its maximum for the laser spot centered at the superlattice and rapidly decays with the spot shifting away. For the beam spot touching the sample edge the current increases again. This is caused by an edge photocurrent [52] known for graphene [53, 54] and semiconductor QWs [55]. Comparison with the laser beam spatial distribution measured by a pyroelectric camera (dashed curve in Fig. 8) shows that the change of the photocurrent for the scans across the DGG structure only slightly deviates from the Gaussian intensity profile. Note that the DGG area is smaller than the beam spot. These findings unambiguously demonstrate that the photocurrent is caused by irradiation of the superlattice.

FIG. 6: Normalized photocurrent \( J_x/P \) measured as a function of magnetic field \( B \) in (Cd,Mn)Te QW sample #4 with the Dy grating.

FIG. 7: (a) Normalized photocurrent \( J_x/P \) as a function of magnetic field \( B \) in CdTe-based QW sample #5 at two gate voltage sequences: \( U_{G1}/U_{G2} = −2.5 \) V/0 and \( U_{G1}/U_{G2} = 0/−2.5 \) V. Panels (b) and (c) show dependencies of the photocurrent magnitude on the gate voltage \( U_{G1} \) (\( U_{G2} \)) obtained for zero potential on the other gate \( U_{G2} \) (\( U_{G1} \)). The data in panels (b) and (c) are obtained for the photocurrent maxima/minima at \( B = −4.9 \) and 4.9 T, respectively.
FIG. 8: Laser spot position dependence of the normalized photocurrent $J_x/P$ measured in (Cd,Mn)Te QW sample #1 at a maximum of the photocurrent oscillation at $B = 4.39$ T and $U_{G1} = 0$, $U_{G2} = -0.5$ V. Inset shows the setup with the laser spot scanned along the $x$-axis. Positions $x_1$ and $x_2$ correspond to the borders of the superlattice whereas $x_3$ denotes the sample edge position. The dashed line represents the laser beam spatial distribution which is measured by a pyroelectric camera and scaled to the current maximum.

C. Effect of the lateral asymmetry variation of the photocurrent

In order to explore the role of the lateral asymmetry, a prerequisite for the ratchet photocurrents, we have systematically studied magneto-photocurrents for different combinations of the gate voltages. The results are shown for different samples in Figs. 3, 4, 7 and 9.

While the magnitude and the sign of the oscillations are strongly affected by the variation of the gate potentials the maxima/minima positions remain unchanged. To show that this conclusion is valid for the whole range of gate potentials used in our measurements we studied the photocurrent for a large set of different magnitudes and polarities of $U_{G1}$ and $U_{G2}$. These results are presented in the inset in Fig. 9 for $B$ ranging from 2.7 to 4.1 T.

Using the fact that maxima positions do not shift upon variation of $B$ we fixed the magnetic field and controlably varied the lateral asymmetry by changing the potential applied to one of the gates and holding the other one at zero bias. Figures 9(a) and 9(b) show the results obtained for (Cd,Mn)Te QW sample #1 at magnetic field strengths 3.9 and $-3.9$ T, respectively. The figures reveal that the polarity of photocurrent changes with the sign of the asymmetry parameter $Ξ$, Eq. (1). This is primarily seen by comparing the curves obtained by variation of the potentials applied either to the thin (dashed lines) or thick (solid lines) gate stripes. The observed stronger change of the signal for $U_{G1}/U_{G2} \approx -0.35$ V corresponds to an increase of the longitudinal resistance detected in magneto-transport measurements, see inset in Fig. 2(b).

It should be noted that, due to the abovementioned built-in potential, the ratchet current can be detected even for zero gate voltages at both gates.

The same behavior upon variation of the lateral asymmetry has been observed for Dy-based DGG sample #4.

Studying the photocurrent as a function of the gate voltage in CdTe QW sample #5 and in (Cd,Mn)Te samples #2 and #3 we obtained, that, despite the background, the photocurrent magnitude is also controlled by the lateral asymmetry. Corresponding results obtained for CdTe QW DGG structure #5 at $B = \pm 4.9$ T are shown in Figs. 7(b) and (c).

Now we turn to the analysis of the $1/B$-oscillations of the photocurrent which are obviously related to the SdH oscillations. Comparison with the magneto-transport data reveals that the period of the $1/B$-oscillations is indeed equal to that of the longitudinal magneto-resistance oscillations. This result is confirmed for all samples and
FIG. 10: Normalized photocurrent $J_x/P$ as a function of $B$ measured in (Cd,Mn)Te QW DGG sample #1 for three temperatures and two gate voltage combinations.

In low-dimensional semiconductor structures with lateral superlattices, a dc electric current is generated due to the action of an electromagnetic wave’s ac electric field [33]. The effect of the superlattice is twofold: It generates a one-dimensional periodic electrostatic potential $V(x)$ acting upon the 2D carriers with $x$ being the superlattice principal axis, and causes a periodic spatial modulation of the THz electric field due to the near field diffraction.

Figure 11 shows coordinate dependence of the THz electric near-field $E_x(x)$ calculated for the (Cd,Mn)Te QWs based DGG structure for two combinations of the gate voltages. The electric field distribution caused by the near-field diffraction is calculated for radiation with frequency $f = 2.54$ THz applying a self-consistent electromagnetic approach based on the integral equation method described in detail in Ref. [56].

Figure 12 shows the calculated THz absorption spectrum of the structure. It is seen that the plasmonic resonances in the QW are excited at frequencies well below the operation frequency of 2.54 THz. Therefore in the experimental frequency range the absorption follows the Drude law, see the inset in Fig. 12. As a result, the near-field distribution in the QW shown in Fig. 11 is caused almost solely by the metal dual-grating gate and not by the plasma oscillations. Hence one can neglect the dependence of the near field on the voltage applied to the DGG. Moreover, since the radiation frequency is much higher than that of plasmonic resonances we consider only electronic ratchet mechanism below.

The ratchet current is generated by a combined action on carriers of both the radiation near field, transmitted through the grating, and the periodic static potential $V(x)$ [14–16, 21, 23]. A crucial condition for dc electric current generation is that the lateral superlattice is asymmetric. Applying the voltages $U_{G1}$ and $U_{G2}$ in a controllable way, one can vary the potential $V(x)$ and reverse the lateral asymmetry $\Xi$. Consequently, the ratchet photocurrent can also reverse its sign as observed in experiment, see Fig. 3.

The ratchet current has components both perpendicular and parallel to the metal fingers and consists, in general, of polarization-independent, linear- and circular-ratchet contributions. All these individual ratchet cur-
FIG. 11: Electric near-field $E_x(x)$ normalized to the electric field of the incident THz wave. Shaded regions correspond to the positions of DGG metal fingers. Results are obtained for parameters of (Cd,Mn)Te QW sample #1 with dielectric constant $\varepsilon = 10$ at the frequency 2.54 THz. The momentum relaxation time $\tau$ is obtained from the electron mobility specified in Sec. II.

FIG. 12: Terahertz absorption spectrum of the structure. The inset shows the spectrum in the vicinity of the frequency 2.54 THz (indicated by vertical arrow) used in our experiments. The curve is calculated for the parameters used in Fig. 11.

Currents have been observed and described in various semiconductor-based structures [14, 15, 21] as well as in graphene with lateral periodical top gates [16, 23]. The mechanism leading to photocurrent formation can be illustrated on the polarization-independent photocurrent caused by the Seebeck ratchet (thermoratchet) effect. This contribution dominates at zero magnetic field (Sec. IV, Fig. 3) and, as we show below, is most relevant to the observed magnetic ratchet current. The Seebeck ratchet effect is caused by inhomogeneous heating of two-dimensional electron gas and subsequent relaxation of the electron temperature. Due to the near-field space modulation, the field $E(x)$ acting upon electrons depends on the coordinate $x$, Fig. 11. The field heats the electron gas changing the effective electron temperature locally to $T(x) = T + \delta T(x)$. Here we assume that, within a short time, the electron distribution becomes a quasi-equilibrium Fermi-Dirac distribution with the temperature $T(x)$. The space-modulated temperature correction is defined by the energy balance and can be found from the following equation [16]

$$\frac{k_B \delta T(x)}{\tau_e} = 2|E(x)|^2 \frac{e^2}{m_0 \omega^2 \tau}. \quad (2)$$

Here $k_B$ is the Boltzmann constant, $\tau_e$ is the temperature relaxation time, $\tau$ is the momentum relaxation time, $e$ is the electron charge, and $m$ is the electron effective mass. We take into account that, in the present experiment $\omega \tau \gg \omega_c \tau \gg 1$, where $\omega_c = |eB|/(mc)$ is the cyclotron frequency.

As a result of the inhomogeneous heating, electrons diffuse from warmer to colder regions, and form a nonequilibrium density profile given by

$$\frac{\delta N(x)}{N} = -\frac{\pi^2}{6} \left( \frac{k_B T}{\varepsilon_F} \right)^2 \frac{\delta T}{T}, \quad (3)$$

where $N$ is the average electron density, $\varepsilon_F$ is the Fermi energy. The ratchet current at zero magnetic field can be represented as a drift current of the electrons in the electric field $\mathcal{E}$ of the space modulated electrostatic potential $V(x)$. From Ohm’s law $j = \sigma \mathcal{E}$ with $\mathcal{E} = -(1/e)dV/dx$ we have

$$j_0 = -\frac{e \tau}{m} \frac{\delta N(x)}{dx} \frac{dV}{dx}. \quad (4)$$
where the bar denotes averaging over the superlattice period. Finally, the ratchet current density at zero magnetic field is given by [16, 33]

\[ j_0 = \frac{\pi e^3 \tau_e k_B T}{3 n h^2 \omega_e \Xi} \Xi, \quad (5) \]

where \( \Xi \) is given by Eq. (1).

Figure 13 shows the photocurrent calculated after Eq. (5) together with the data of Fig. 3. The result of Fig. 13 is obtained for the near-field \( E_x(x) \) shown in Fig. 11. Parameters used for the calculations correspond to the sample #1. The only adjustable parameter is the temperature relaxation time \( \tau_e \) taken as 4 ns. This value agrees with the temperature relaxation time of few nanoseconds reported for a degenerate electron gas in GaAs-based heterojunctions [57]. Figure 13 shows qualitative and reasonably good quantitative agreement between theory and experiment.

The above analysis suggests that, in the absence of magnetic field, the ratchet current is rather weak for degenerate electrons because, according to Eq. (3), the relative concentration correction \( \delta N/N \) is much smaller than the temperature correction \( \delta T/T \). Below we show that the situation changes drastically in the presence of a quantizing magnetic field \( B \parallel z \).

The magnetic field induced ratchet currents in the directions perpendicular, \( j_x \), and parallel, \( j_y \), to the stripes of the superlattice are given by [33]

\[ \frac{j_x}{j_0} = \frac{48 \varepsilon_F^2}{h \omega_e k_B T} \frac{(\omega_e \tau)^2}{1 + (\omega_e \tau)^2} \sinh z - z \cosh z \frac{\sinh^2 z}{\sinh^2 z} \delta, \quad (6) \]

\[ j_y = \frac{B_z}{|B_z|} \frac{1 + 3(\omega_e \tau)^2}{2(\omega_e \tau)^3} j_x. \quad (7) \]

Here the magneto-oscillations are described by the factor \( \delta \) (\( |\delta| \ll 1 \))

\[ \delta = \cos \left( \frac{2 \pi \varepsilon_F}{h \omega_e} \right) \cos \left( \frac{\pi \Delta Z}{h \omega_e} \right) \exp \left( - \frac{\pi}{\omega_e \tau} \right), \quad (8) \]

while the dependence on \( z = 2 \pi^2 k_B T/(h \omega_e) \) describes the oscillation suppression with increasing temperature. Eqs. (5)-(7) are derived in the first order in \( \delta \). As compared with the theory developed in Ref. [33] we take into account the spin subband splitting \( \Delta Z \) due to the Zeeman effect. For the DMS based ratchet structures the exchange enhanced Zeeman splitting is given by [38, 41]

\[ \Delta Z = g^* \mu_B B + \bar{x} S_0 N_0 \alpha_e B_{5/2} \left( \frac{5 \mu_B g_m^* B}{2 k_B (T_{\text{Mn}} + T_0)} \right) \quad (9) \]

where \( g^* \) is the electron Landé factor in the absence of magnetic impurities, \( \mu_B \) is Bohr’s magneton, \( g_m^* = 2 \) is the Mn-g-factor, \( T_{\text{Mn}} \) is the Mn-spin system temperature, \( S_0 \) and \( T_0 \) account for the Mn-Mn antiferromagnetic interaction, \( B_{5/2}(\xi) \) is the modified Brillouin function, and \( N_0 \alpha_e \) is the exchange integral. Equations (6), (7) predict that the ratchet current components \( j_x \) and \( j_y \propto j_x B_z \) have opposite parity upon magnetic field reversal due to the photocurrent deflection by the Lorentz force [58].

The ratchet current becomes an oscillating function of the magnetic field as the Landau levels move through the Fermi level and the photocurrent \( 1/B \)-oscillation period is the same as for SdH oscillations. Equation (6) explains the reason for the ratchet current oscillations with giantly enhanced magnitude as compared to the ratchet current at zero magnetic field. The crucial issue is that the ratchet current in a quantized magnetic field arises due to heating-induced corrections to the conductivity rather than a variation of the electron density, and the conductivity in this regime is extremely sensitive to electron temperature variations. Indeed, even a weak change of the electron temperature near the Dingle temperature results in exponentially strong changes of the conductivity [59]. Therefore, the sensitivity of the conductivity to electron gas heating results in a huge enhancement of the ratchet current. The ratio \( j(B)/j_0 \) is governed by a factor \( (\varepsilon_F/k_B T)(\varepsilon_F/h \omega_e) \gg 1 \) and can reach about two orders of magnitude [33]. It should be stressed that this enhancement occurs in moderate fields where the resistance exhibits weak SdH oscillations. Heating damps the conductivity oscillations, therefore, depending on the sign of the correction, heating can either increase or decrease the conductivity because \( (\partial \sigma/\partial T) \) changes sign as a function of \( B \). As a result, the heating-induced ratchet current is an oscillating function of the field with a zero mean value.

The calculated magnetic field dependence of the ratchet currents \( j_x \) and \( j_y \) are shown in Fig. 14. The results are presented for two gate voltage combinations with equal magnitude but opposite sign of \( \Xi \). Equations (5)-(7) reveal the most important features of the magnetic ratchet effect: the current is proportional to |\( E_0 \)|, oscillates around zero with the same period as the longitudinal magnetoresistance, the amplitude of the current oscillations is immensely larger than the ratchet current at zero magnetic field, and the sign of the photocurrent reverses by changing the sign of \( dV/dx \). All these features have been observed experimentally, see Figs. 4-7, 9, and 10.

Equations (6)-(8) also describe the more complicated oscillating ratchet current behavior observed in the DMS structures at low temperatures, see Figs. 10 and 15 for experiment and theory, respectively. Indeed, due to the temperature dependence of the Brillouin function at low temperatures the Zeeman splitting becomes comparable to the Landau levels separation. Calculated curves for three values of the lattice temperatures and, consequently, different contributions of the Zeeman effect, are shown in Fig. 15. The calculations show, as in experiment, beats in the oscillations of \( j_x(B) \). They stem from the interplay of Zeeman and Landau splittings and become more pronounced with temperature decreasing. Comparison of Figs. 10 and 15 demonstrates that
Fig. 14: Photocurrents $j_x$ and $j_y$ calculated after Eqs. (6), (7) for (Cd,Mn)Te QW sample at $T = 4.2$ K. The structure parameters are relevant to the experiment presented in Fig. 4: $\varepsilon_F = 13$ meV, $\mu = 0.95 \times 10^8$ cm$^2$/Vs and $\bar{x} = 0.015$. For other parameters we used the literature values for n-(Cd,Mn)Te: $g^* = -1.64$, $N_0\alpha_e = 220$ meV, see Ref. [41], and $m = 0.1m_0$, see Ref. [60]. For the calculations we also used $T_{\text{Mn}} = T$ and literature data of $T_0 = 0.8$ K and $S_0 = 2.2$ for $\bar{x} = 0.015$, see Ref. [61]. Solid and dashed curves show the results for two asymmetries of equal magnitudes but opposite signs of $\Xi$. The oscillation amplitude is much higher than the ratchet current $j_0$ at zero magnetic field (the latter is not seen at the chosen scale).

Eq. (6) describes the qualitative behavior of the photocurrent quite well. We note that the beats in $j_{x,y}(B)$ are substantially influenced by the Mn spin system temperature, which, because of electron gas heating, can be higher than the lattice one [62]. This increase due to the strong dependence of the Brillouin function on $T_{\text{Mn}}$, results in a reduced exchange part of $\Delta Z$ in Eq. (9). This shifts the onset of the exchange enhanced Zeeman splitting to higher magnetic fields. Allowance for this effect should further improve the agreement between experimental data and calculations.

VII. SUMMARY

To summarize, we have experimentally demonstrated and theoretically explained the magnetic quantum ratchet effect, i.e., the ratchet effect in quantizing magnetic fields. To generate the ratchet current we use an asymmetric interdigitated top gate superlattice on top of the investigated quantum wells. Electric currents driven by terahertz electric field exhibit sign-changing magneto-oscillations with an amplitude giantly enhanced as compared to the photocurrent at zero magnetic field. The current amplitude and direction can be controllably changed by the variation of voltages applied to individual gate sublattices. The effect is observed in structures with various QW compositions and superlattice parameters. The photocurrent generation mechanism can be well described in terms of semiclassical theory of magnetic ratchet effects. The observed effect is driven by the periodic modulation of the electron temperature caused by near field diffraction. The theory of the Seebeck ratchet effect in the presence of quantizing magnetic field shows that the ratchet current follows the oscillations of the longitudinal resistance. In the DMS structures at low temperatures the investigated effect is strongly influenced by the exchange enhanced Zeeman splitting caused by the exchange interaction of electrons with Mn$^{2+}$ ions.

Finally we note, that while here we have dealt with a homogeneous magnetic field, the observed ratchet photocurrent in superlattices made of hard magnetic material (Dy) opens a possibility to study the ratchet effect driven by an inhomogeneous periodic magnetic field recently suggested in Ref. [33, 45]. This kind of experiments would apply remnant magnetization of Dysprosium together with the enhanced magnetic properties of DMS QWs and is a future task.

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[1] F. Jülicher, A. Ajdari, and J. Prost, Rev. Mod. Phys. 69, 1269 (1997).
[2] P. Reimann, Phys. Rep. 361, 57 (2002).
[3] H. Linke (ed.), Ratchets and Brownian Motors: Basics, Experiments and Applications, special issue Appl. Phys. A: Mater. Sci. Process. A 75, 167 (2002).
[4] P. Hänggi and F. Marchesoni, Rev. Mod. Phys. 81, 387 (2009).
[5] S. Denisov, S. Flach, and P. Hänggi, Phys. Rep. 538, 77 (2014).
[6] M. Büttiker, Z. Phys. B 68, 161 (1987).
[7] Ya. M. Blanter and M. Büttiker, Phys. Rev. Lett. 81, 4040 (1998).
[8] P. Reimann, M. Grifoni, and P. Hänggi, Phys. Rev. Lett. 79, 10 (1997).
[9] A. Lorke et al., Physica B 249, 312 (1998).
[10] A. M. Song et al., Phys. Rev. Lett. 91, 1357 (2001).
[11] A. D. Chepelianski, M. V. Entin, L. I. Magarill, and D. L. Shepelyansky, Eur. Phys. J. B 56, 323 (2007).
[12] A. D. Chepelianski, M. V. Entin, L. I. Magarill, and D. L. Shepelyansky, Eur. Phys. J. B 56, 102 (2007).
[13] S. Denisov, S. Flach, and P. Hänggi, Phys. Rep. 538, 77 (2014).
[14] P. Olbrich, E. L. Ivchenko, R. Ravash, T. Feil, S. N. Danilov, J. Allerdings, D. Weiss, D. Schuh, W. Wegscheider, and S. D. Ganichev, Phys. Rev. Lett. 103, 690603 (2009).
[15] E. L. Ivchenko and S. D. Ganichev, Pisma v ZhETF 93, 752 (2011) [JETP Lett. 93, 673 (2011)].
[16] A. V. Naïlov, L. E. Golub, and E. L. Ivchenko, Phys. Rev. B 86, 115301 (2012).
[17] V. V. Popov, Appl. Phys. Lett. 102, 253504 (2013).
[18] S. V. Koniakhin, Eur. Phys. J. B 56, 32 (2007); Physica E (Amsterdam) 40, 1264 (2008).
[19] S. Sassine, Yu. Krupko, J.-C. Portal, Z. D. Kvon, R. Murali, K. P. Martin, G. Hill, and A. D. Wieck, Phys. Rev. B 78, 045431 (2008).
[20] P. Olbrich, E. L. Ivchenko, R. Ravash, T. Feil, S. N. Danilov, J. Allerdings, D. Weiss, D. Schuh, W. Wegscheider, and S. D. Ganichev, Phys. Rev. B 91, 235436 (2015).
[21] P. Olbrich, J. Karch, E. L. Ivchenko, J. Kamann, B. März, M. Feihrenbacher, D. Weiss, and S. D. Ganichev, Phys. Rev. B 83, 165320 (2011).
[22] E. S. Kannan, I. Bisotto, J.-C. Portal, T. J. Beck, and L. Jalabert, Appl. Phys. Lett. 101, 143504 (2012).
[23] P. Olbrich, J. Kamann, M. König, J. Munzert, L. Tutsch, J. Eroms, D. Weiss, M.-H. Liu, L. E. Golub, E. L. Ivchenko, V. V. Popov, D. V. Fateev, K. V. Mashinsky, F. Fromm, Th. Seyller, and S. D. Ganichev, Phys. Rev. B 93, 075422 (2016).
[24] C. Drexler, S. A. Tarasenko, P. Olbrich, J. Karch, M. Hirmer, F. Müller, M. Gmitra, J. Fabian, R. Yakinova, S. Lara-Avila, S. Kubatkin, and S. D. Ganichev, Nat. Nanotechn. 8, 104 (2013).
[25] T. Watanabe, S. A. Bouanga-Tombet, Y. Tanimoto, D. Fateev, V. Popov, D. Coquillat, W. Knap, Y. M. Meziani, Yuye Wang, H. Minamide, H. Ito, and T. Otsuij, IEEE Sensors J. 3, 89 (2013).
[26] Y. Kurita, G. Ducournau, D. Coquillat, A. Satou, K. Kobayashi, S. Bouanga Tombet, Y. M. Meziani, V. V. Popov, W. Knap, T. Suemitsu, and T. Otsuij, Appl. Phys. Lett. 104, 251114 (2014).
[27] S. A. Bouanga-Tombet, Y. Tanimoto, A. Satou, T. Suemitsu, Y. Wang, H. Minamide, H. Ito, D. V. Fateev, V. V. Popov, and T. Otsuij, Appl. Phys. Lett. 104, 262104 (2014).
[28] V. V. Popov, D. V. Fateev, T. Otsuij, Y. M. Meziani, D. Coquillat, and W. Knap, Appl. Phys. Lett. 99, 243504 (2011).
[29] P. Faltermeier, P. Olbrich, W. Probst, L. Schell, T. Watanabe, S. A. Bouanga-Tombet, T. Otsuij, and S. D. Ganichev, J. Appl. Phys. 118, 084301 (2015).
[30] S. D. Ganichev, W. Weber, J. Kiermaier, S. N. Danilov, D. Schuh, W. Wegscheider, Ch. Gerl, D. Bougeard, G. Abstreiter and W. Prettl, J. Appl. Physics 103, 114504 (2008).
[31] S. N. Danilov, B. Wittmann, P. Olbrich, W. Eder, W. Prettl, L. E. Golub, E. V. Beregulín, Z. D. Kvon, N. N. Mikhailov, S. A. Dvoretsky, V. A. Shalygin, N. Q. Vinh, A. F. G. van der Meer, B. Murdin, and S. D. Ganichev, J. Appl. Phys. 105, 013106 (2009).
[32] S. Dvoretsky, N. Mikhailov, Y. Sidorov, V. Shvets, S. Danilov, B. Wittman, and S. Ganichev, J. Electron. Mat. 39, 918 (2010).
[33] G. V. Budkin, L. E. Golub, E. L. Ivchenko, and S. D. Ganichev, JETP Lett. 104, 649 (2016).
[34] S. A. Crooker, D. A. Tuchinsky, J. Levy, D. D. Awschalom, R. Garcia, and N. Samarth, Phys. Rev. Lett. 75, 505 (1995).
[35] J. C. Egues and J. W. Wilkins, Phys. Rev. B 58, R16012 (1998).
[36] J. Jaroszynski, T. Andrareczyk, G. Karczewski, J. Wróbel, T. Wojtowicz, E. Papis, E. Kaminska, A. Potrowska, D. Popovic, and T. Dietl, Phys. Rev. Lett. 89, 266802 (2002).
[37] S. D. Ganichev, S. A. Tarasenko, V. V. Bel’kov, P. Olbrich, W. Eder, D. R. Yakovlev, V. Kolkovsky, W. Zaczeszczuk, G. Karczewski, T. Wojtowicz, and D. Weiss, Phys. Rev. Lett. 102, 156602 (2009).
[38] P. Olbrich, C. Zoth, P. Lutz, C. Drexler, V. V. Bel’kov, Ya. V. Terent’ev, S. A. Tarasenko, A. N. Semenov, S. V. Ivanov, D. R. Yakovlev, T. Wojtowicz, U. Wurstbauer, D. Schuh, and S. D. Ganichev, Phys. Rev. B 86, 085310 (2012).
[39] M. K. Kneip, D. R. Yakovlev, M. Bayer, G. Karczewski, T. Wojtowicz, and J. Kossut, Appl. Phys. Lett. 88, 152105 (2006).
[40] J. A. Gaj, R. Planal, and G. Fishman, Solid State Commun. 29, 435 (1979).
[41] J. K. Furdyna, J. Appl. Phys. 64, R29 (1988).
[42] T. Dietl, in Handbook on Semiconductors, vol. 3b, Ed.
T.S. Moss (North-Holland, Amsterdam, 1994).

[43] *Introduction to the Physics of Diluted Magnetic Semiconductors*, Eds. J. Kossut and J. A. Gaj (Springer, Berlin 2010).

[44] M. Staab, M. Matuschek, P. Pereyra, M. Utz, D. Schuh, D. Bougeard, R. R. Gerhardt, and D. Weiss, New J. Phys. 17, 043035 (2015).

[45] G.V. Budkin, and L.E. Golub, Phys. Rev. B 90, 125316 (2014).

[46] J. Karch, P. Olbrich, M. Schmalzbauer, C. Zoth, C. Brinsteiner, M. Fehrenbacher, U. Wurstbauer, M. M. Glazov, S. A. Tarasenko, E. L. Ivchenko, D. Weiss, J. Eroms, and S. D. Ganichev, Phys. Rev. Lett. 97, 227402 (2010).

[47] Z. D. Kvon, S. N. Danilov, N. N. Mikhailov, S. A. Dvoretzky, and S. D. Ganichev, Physica E 40, 1885 (2008).

[48] E. Ziemann, S. D. Ganichev, I. N. Yassievich, V. I. Perel, and W. Prettl, J. Appl. Phys. 87, 3843 (2000).

[49] Note that in $x$-direction the polarization independent contribution $J^D_x$ dominates the photocurrent for all studied samples and almost all combinations of gate voltages applied to the individual subgratings of DGG.

[50] Fabrication of such a large-size superlattices is a challenging task. Therefore, some of our structures have minor imperfections, as confirmed by optical microscope images. The imperfections occur on samples with occasional inhomogeneities of the PMMA resist. Due to that the electron beam lithography was unable to write the exact width of the stripes as it was intended and, therefore, ended up with an overlap of the Au fingers. This leads to short circuits, as well as to complete destruction of few gate fingers by removing the additional Au material in the finger spacings. In some of our structures the connection between two gate stripes also showed up when surface impurities were covered with Au, which were not supposed to be part of the gate fingers.

[51] V. V. Bel’kov and S. D. Ganichev, Semicond. Sci. Technol. 23, 114003 (2008).

[52] The edge photocurrent is caused by the asymmetric scattering of carriers driven back and force to the edge by the radiation electric field [53, 54].

[53] J. Karch, C. Drexlter, P. Olbrich, M. Fehrenbacher, M. Hirmer, M. M. Glazov, S. A. Tarasenko, E. L. Ivchenko, B. Bärfinger, J. Eroms, D. Weiss, R. Yakimova, S. Lara-Avila, S. Kubatkin, M. Ostler, T. Seyller, and S. D. Ganichev, Phys. Rev. Lett. 107, 276601 (2011).

[54] M. M. Glazov and S. D. Ganichev, Physics Reports 535, 101 (2014).

[55] K.-M. Dantscher, D. A. Kozlov, M. T. Scherr, S. Gebert, J. Bärfinger, M. V. Durnev, S. A. Tarasenko, V. V. Bel’kov, N. N. Mikhailov, S. A. Dvoretzky, Z. D. Kvon, D. Weiss, and S. D. Ganichev, arXiv cond-mat: 1612.08854 (2016).

[56] D. V. Fateev, V. V. Popov, and M. S. Shur, Semicond. 44, 1406 (2010).

[57] T. Kawamura, S. Das Sarma, R. Jalabert, and J. K. Jain, Phys. Rev. B 42, 5407 (1990).

[58] K.-M. Dantscher, D. A. Kozlov, P. Olbrich, C. Zoth, P. Faltermeier, M. Lindner, G. V. Budkin, S. A. Tarasenko, V. V. Bel’kov, Z. D. Kvon, N. N. Mikhailov, S. A. Dvoretzky, D. Weiss, B. Jenichen, and S. D. Ganichev, Phys. Rev. B 92, 165314 (2015).

[59] C. Hamaguchi, *Basic Semiconductor Physics* (Springer 2014).

[60] A. A. Dremin, D. R. Yakovlev, A. A. Sirenko, S. I. Gubarev, O. P. Shabelsky, A. Waag, and M. Bayer, Phys. Rev. B 72, 195337 (2005).

[61] W. J. Ossau and B. Kuhn-Heinrich, Physica B 184, 422 (1993).

[62] D. Keller, D. R. Yakovlev, B. König, W. Ossau, Th. Gruber, A. Waag, L. W. Molenkamp, and A. V. Scherbakov, Phys. Rev. B 65, 035313 (2002).