Controlling circular polarization of light emitted by quantum dots using chiral photonic crystal slab

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We study the polarization properties of light emitted by quantum dots that are embedded in chiral photonic crystal structures made of achiral planar GaAs waveguides. A modification of the electromagnetic mode structure due to the chiral grating fabricated by partial etching of the waveguide layer has been shown to result in a high circular polarization degree ρc of the quantum dot emission in the absence of external magnetic field. The physical nature of the phenomenon can be understood in terms of the reciprocity principle taking into account the structural symmetry. At the resonance wavelength, the magnitude of |ρc| is predicted to exceed 98%. The experimentally achieved value of |ρc| = 81% is smaller, which is due to the contribution of unpolarized light scattered by grating defects, thus breaking its periodicity. The achieved polarization degree estimated removing the unpolarized nonresonant background from the emission spectra can be estimated to be as high as 96%, close to the theoretical prediction.

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I. INTRODUCTION

The possibility to control the polarization state of radiation from quantum emitters has drawn attention of researchers in recent years as it opens various important applications in spin-optoelectronics, quantum information technology, chiral synthesis and sensing. A common way for polarization conversion and rotation is the use of wave plates of birefringent materials and optical gratings. An imbalance between the left- and right-circularly polarized photons takes place in chiral materials with nonequivalent left- and right-circularly polarized electromagnetic field modes.1–4 The imbalance in semiconductors is usually reached by applying a static magnetic field that disturbs the time-reversal symmetry and leads to a splitting of the left- and right-circularly polarized modes.

Advances in nanoscale fabrication have made it possible to realize artificial photonic structures with desired symmetry and density of the environmentally allowed electromagnetic modes, which allows to control the spontaneous emission rate of emitted light, its radiation pattern and direction. Moreover, the fabrication of chiral nanostructures from achiral semiconductor materials opens the possibility to control the polarization of emitted light,5 as the polarization effects are determined by the overall structure symmetry. This method has considerable advantages in comparison with the others as it is compatible with semiconductor technology and allows to fabricate nanoscale devices (thickness of a conventional quarter-wave plate is much larger) with a simple operation (external magnetic field application is not easy).

Recently Konishi et al.5 fabricated a simple chiral nanostructure that consisted of InAs quantum dots (QDs) embedded in the waveguide region of a planar GaAs based dielectric waveguide coupled to a dielectric chiral photonic crystal slab (CPCS), and obtained a degree of circular polarization of QD emission ρc = 26%. A significantly higher value of ρc of QD emission (up to 70% in the direction normal to the structure plane and up to 81% at some angle) was experimentally achieved from a planar semiconductor microcavity with chiral partially etched top mirror,6 but this structure is far more complex. The degree of circular polarization of emission from a chiral structure made of achiral semiconductors depends strongly on its geometry and the radiation frequency, which allows one to optimize the structures. Recent numerical simulations5,6 show that values of ρc as high as 98 and 99% in waveguide and microcavity structures, respectively, can be reached by their optimization.

In this paper, we have experimentally investigated the polarization of emission of InAs QDs embedded in a planar GaAs based dielectric waveguide coupled to a dielectric chiral photonic crystal slab with sub-wavelength period in order to reach the predicted high values of ρc. The structure geometry has been optimized on the base of the computation of the QDs radiation performed using...
an oscillating point dipole model. A circular polarization degree of InAs QD emission in the finite (NA less than 0.02) aperture as high as 81% is experimentally realized in fabricated optimized structures. The achieved value is found to be limited by the unpolarized scattered light background caused by the fluctuations in the periodic potential due to the size and shape imperfections of etched rectangular pillars in the chiral layer. It is worthwhile to note that the magnitude of ρc obtained from the spectra with canceled background due to the lattice imperfection reaches 96%. Thus, the considered very simple chiral structure made of conventional achiral semiconductor materials using the chiral morphology effect can enable the fabrication of compact solid state circularly polarized light-emitting devices with future progress in fabrication technology.

We would like to add that recently, a possibility to control deterministically the direction of photon emission (depending on the handedness of its circular polarization) by a QD inside a chiral photonic crystal waveguide has been demonstrated. Our structure with randomly distributed QDs may open an alternative way to this goal, being not sensitive to the exact positioning of the emitting QDs inside the structure.

The paper is organized as follows: The experimental details and the sample are described in Sec. II. The experimental results are described in Sec. III. The physical nature of the effect is discussed in Sec. IV. Section V contains the concluding remarks.

II. EXPERIMENT

The epitaxial layer structure, which formed the basis of this study, consisted of a 691 nm thick GaAs membrane with a single layer of embedded randomly distributed InAs quantum dots (Fig. 1a). The membrane is grown on top of a 1 µm thick AlGaAs buffer layer. We fabricated an array of nano-pillars into the upper nominally 428 nm thick part of the membrane layer via electron beam lithography and reactive ion etching. The nano-pillars were arranged into a square lattice of unit cells consisting of four rectangular pillars, each rotated by 90° with respect to its nearest neighbors. The lattice period p was varied in the range of 0.7–1.1 µm. The unit cell is shown in Fig. 1b. The distance between pillars was p/5, their sides were p/5 and 2p/5, respectively. Both right and left (mirrored) twisted pillars were manufactured. (For definiteness, we call hereinafter the structures shown in Figs. 1, 2 as right-twisted.) The thickness of GaAs waveguide layer (εGaAs = 12.42), containing a plane with QDs was 263 nm. The plane with QDs was located 100 nm above its bottom. The lower Al0.7Ga0.3As (εAlGaAs = 9.66) buffer layer was 1 µm thick. The whole system was grown by molecular beam epitaxy on a GaAs substrate. Representative SEM pictures of the right-twisted chiral photonic layer are shown in Fig. 2.

The sample was at a temperature of 5 K in the insert of an optical cryostat. The luminescence polarization was analyzed by a quarter wave retarder and linear polarizers. The angle resolution of 0.5° is ensured by a small aperture. The circular polarization degree of the luminescence from the structure prior to etching was less than 0.1%.
III. EXPERIMENTAL RESULTS

Experimental circularly polarized spectra of QD emission are shown in Fig. 3 (left axis) for left and right-twisted rectangular pillars. The green lines in Fig. 3, right axes, show the resulting spectra of the circular polarization degree of emission

\[
\rho_c = \frac{I^+ - I^-}{I^+ + I^-},
\]

where \(I^\pm\) is the emission intensity in right/left circular \(\sigma^\pm\)-polarization. The spectra are recorded in the direction \(z\) (perpendicular to the structure plane) with numerical aperture NA=0.005. For comparison, the calculated emission spectra in \(\sigma^\pm\) polarization and \(\rho_c\) are shown in Fig. 4 for the right-twisted structure with the same parameters. The spectra were calculated using the reciprocity principle and the optical scattering matrix method.\(^{8,9}\) Compared to Ref. 9, we changed the parameters of the materials, because the current experiment is carried out at low rather than at room temperature.

Figure 3 shows that, in accordance with the calculations, the polarization of the emission line at the resonance frequency is opposite in the structures with the left and right-twisted pillars.

The experimental and calculated dependencies in Figs. 3 and 4 are in a good qualitative agreement. A small 9 nm red shift of the calculated resonance wavelength is most probably due to a slightly incorrect dielectric susceptibilities used in the calculations, the agreement can be easily improved by their fitting.

Note, however, that (i) the experimental line FWHM is about 5 times greater than the calculated one (\(\approx 4\) and 0.8 nm, respectively), and (ii) the line sits on a background whose magnitude is about 9% from its peak intensity whereas the background in the calculated spectra does not exceed 1%. Both the line broadening and background magnitude are found to depend strongly on the pillar quality, which indicates small deviations from the ideal structure. Figure 5 shows that magnitudes of \(\rho_c = -0.81\) and \(+0.67\) in the waveguides with the right and left-twisted pillars are limited by the unpolarized background. It is worthwhile to note that the magnitude of \(|\rho_c|\) at the resonance reaches 0.96 when this unpolarized background is removed as shown in Fig. 5. This value is very close to the calculated one, which indicates that the predicted values of \(|\rho_c|\approx 0.98\) could be reached due to further advances in fabrication technology.
IV. DISCUSSION

A. Angular dependencies of emission intensities, \( \rho_c \), and the quasiguided modes

As already discussed, the peaks in the QD emission spectrum are due to the excitation of lossy quasiguided modes in the GaAs waveguide inside a periodically modulated structure. Their expected angular dispersion is shown in Fig. 6, where false colors show the calculated intensity of the emission (in \( \sigma^- \) polarization) from the right-twisted structure with period \( p = 770 \) nm as a function of energy (wavelength) and polar angle \( \theta \) in \( M - \Gamma \) (diagonal) and \( \Gamma - X \) directions. These Bragg resonances can be understood as corresponding approximately to the folding of the dispersion of the guided modes into the 1st Brillouin zone (BZ) of the 2D grating (square lattice in our case).

\[
E_{l,m}(k) = \frac{\hbar c}{n_{\text{eff}}} \sqrt{(k_x + l K_{\text{BZ}})^2 + (k_y + m K_{\text{BZ}})^2}, \quad (2)
\]

where \( k = (k_x, k_y) \) is the in-plane wavevector, \( K_{\text{BZ}} = 2\pi/p \) is the Bragg wavenumber, \( p \) is the period, \( n_{\text{eff}} \) is the effective refractive index of the guided mode, \( l \) and \( m \) are integers. It appears that the resonance of interest at \( \lambda_0 \sim 901 \) nm in the current structure corresponds to a fourfold degenerate \( l, m = \pm 2 \) state in the \( \Gamma \)-point (in the scalar approximation and neglecting the energy splitting due to the point symmetry group), see Fig. 6. It is also in agreement with the analysis of Ref. 9, see, e.g., the calculated in-plane distribution of the emission intensity in the dominant polarization in Fig. 6b of Ref. 9.

The degeneracy of the state \( E_{\pm 2, \pm 2} \) is lifted at \( k \neq 0 \). According to Eq. 2 near the \( \Gamma \)-point

\[
E_{l,m}(k) = E_0 + \frac{\hbar c (lk_x + mk_y)}{n_{\text{eff}} \sqrt{l^2 + m^2}} + O(k_x^2 + k_y^2), \quad (3)
\]

where \( E_0 \) is the resonance energy in the \( \Gamma \)-point, \( E_0 = E_{\pm 2, \pm 2}(k = 0) \). Thus, in the \( 0 - X, 0 - Y \) directions, according to Eq. 3, the \( (\pm 2, \pm 2) \) modes split into two degenerate doublets with nearly linear \( k \)-dispersion \( E - E_0 = \pm \hbar c k_{x,y}/(\sqrt{2} n_{\text{eff}}) \). In the diagonal directions, the modes with \( l = m = \pm 2 \) split into two singlets with nearly linear dispersion \( E - E_0 = \pm \hbar c k_{x,y}/n_{\text{eff}} \), whereas those with \( l = -m = \pm 2 \) is a degenerate parabolic doublet with an effective mass \( m_{\text{eff}} \sim 10^{-5} m_e \), where \( m_e \) is the free electron mass. Thus, the modes with \( l = -m = \pm 2 \) are nearly dispersionless at small \( k \lesssim 0.2 \mu m^{-1} \). As a result, the lines of equal energy at \( E = E_0 \) are two mutually perpendicular lines at \( k_y = \pm k_x \) in this range of \( k \). That is well seen in Figs. 7, d representing the measured an-
FIG. 7. (Color online) Polar plots of the measured (left panels) and calculated (right panels) angle dependencies of the QD emission intensities in left and right circular polarizations. The measured spectra were recorded for the resonance wavelength $\lambda_0 = 901.1$ nm (panels c and d), corresponding to the $(\pm 2, \pm 2)$ Bragg resonance at $E = E_0$ (see in the text). Panels (a,b) and (e,f) show the corresponding dependencies for $\lambda_0 - 3.4$ and $+2.6$ nm. The simulated spectra were calculated around the theoretical resonance wavelength $\lambda_{0,\text{th}} = 910.5$ nm (panels i and j). Panels (g,h) and (k,l) show the corresponding dependencies for $\lambda_{0,\text{th}} \pm 3$ nm.

gular distribution of the QD emission near $\theta = 0$ in two circular polarizations at the resonance wavelength.

Figures 7a,b and e,f show that these lines at $E \neq E_0$ split into doublets $k_y = k_x \pm \Delta k$ and $k_y = -k_x \pm \Delta k$ in accordance with the $D_4$ point group symmetry of the modes' dispersion at the $\Gamma$ point.

The measured angular distributions of the emission intensities in $\sigma^\pm$ polarizations and of the circular polarization degree (left panels of Figs. 8 and 9 respectively) are in a good qualitative agreement with the calculated ones displayed in the right panels. It is seen in Fig. 8 that, in agreement with the calculation, the strongest emission in the dominated ($\sigma^-$) polarization is at the crossing of the isoenergetic lines and reaches its maximum at $E = E_0$ when the state at $k = 0$ becomes fourfold degenerate. According to calculations shown in Fig. 9 the QD emission intensity in the dominating left polarization at the resonance $E = E_0$ exceeds that in vacuum more than 30 times, whereas that in the opposite polarization is strongly (about 3 times) depressed. The effect is connected to a modification of the environmentally allowed electromagnetic modes by the CPCS in $k$-space. As a consequence, it is very sensitive to the quality of the photonic crystal. Any disturbance of the potential periodicity results in the increased Rayleigh scattering contributing to $k = 0$ emission in the suppressed polarization. The result is the decreased degree of circular polarization in the experiment.

B. Symmetry analysis and the physical origin of circularly polarized emission

Although the possibility to obtain nearly 100% circularly polarized emission from unpolarized emission of randomly distributed QD was already demonstrated numerically[22] the physical mechanism of this effect has not been yet clarified. The key property of the structure that helps to understand this mechanism is the expected theoretically oscillatory dependence of the degree of circular polarization of emission of such structures on the thickness of the chiral photonic slab thickness, illustrated in Fig. 8. While the calculated dependencies of the emission intensities in right and left polarization $I^\pm$ on $L$ (see Fig. 9) consist of series of at first sight incoherent peaks, the dependence $\rho_c(L)$ (see green line in Fig. 9b) looks as coherent Fabry-Perot oscillations. In what follows, based on the reciprocity and symmetry properties of our struc-
tecture, we show that the chiral photonic crystal slab in the structure of interest plays the role of a wave plate. It introduces a phase shift, proportional to $\Delta K_z L$ ($L$ is the CPCS thickness), between the propagating modes with a large (of the order of $k_0 = \omega/c$) difference of wavenumbers $\Delta K_z$. We will show that these modes are basically different waveguide modes in the GaAs rectangular vertical waveguides, i.e., in the building blocks of the CPCS. There is also a large constant phase shift between left and right circular polarizations, due to the absence of horizontal mirror symmetry of the photonic crystal slab with different top and bottom boundaries (air/CPCS and CPCS/GaAs, respectively). As a result, the transmission of the CPCS in left and right polarizations oscillate as a function of $L$ in counter-phase, which opens a way to reach nearly 100% polarization selectivity.

1. Reciprocity principle for the structures with $C_4$ and $D_4$ symmetry

The emission intensity of QDs can be calculated directly or using the electromagnetic reciprocity principle. In the latter case, the emission problem of randomly distributed and randomly polarized oscillating dipoles is replaced by an illumination problem, in which the structure is illuminated by a polarized plane wave $E_{in}(x,y,z) = E \text{e}^{i k_0 z - i \omega t}$. (Hereinafter index $j$ marks the polarization state, e.g., $j = x, y$ in case of linear polarization along $x, y$, respectively, and $j = \pm$ for right and left polarization.) Then, the resulting electric field distribution in the layer with QD,

$$I^j = \iint dx dy \left( |E_{xj}^2| + |E_{yj}^2| \right),$$

(4)

gives the corresponding polarized component of the QD radiation intensity.

The reciprocity principle helps to understand easily, why in the structure with a $C_4$ symmetry, the emission of QD in the vertical direction cannot be linearly polarized, and why for a structure with higher symmetry (e.g., $D_4$), it cannot be also circularly polarized.

Assume $\mathbf E(x,y,z)$ and $\mathbf H(x,y,z)$ are the solutions of Maxwell’s equations for the system with $C_4$ symmetry. Then, the electromagnetic field rotated by $90^\circ$ is also a solution. The $90^\circ$ rotation switches the linear polarization of the illuminated plane wave $j = x$ to the orthogonal polarization $j = y$, while the integral (4) does not change, $I^x = I^y$. Because of the Eq. (4), $\rho_{xy} = (I^x - I^y)/(I^x + I^y) = 0$, hence the emission cannot be linearly polarized.

Similarly, if a structure has a $D_4$ symmetry (equivalent to $C_{4v}$), Maxwell’s equations are invariant also under mirror reflection operation, e.g., in $XOZ$ plane, which switches the sense of circular polarization of the illuminated plane wave $j = \pm$ to the opposite one, $j = \mp$, while the integral (4) does not change, $I^+ = I^-$. Thus, again, the degree of circular polarization of emission $\rho_c = (I^+ - I^-)/(I^+ + I^-) = 0$, hence the emission cannot be circularly polarized, too.
2. $S$-matrix approach and $C_4$ symmetry

In the structure of interest with $C_4$ symmetry, a layer with randomly distributed and randomly polarized QD is placed in the planar GaAs waveguide. Two lower effective dielectric permittivity layers operate as mirrors. The bottom mirror is the Al$_{0.7}$Ga$_{0.3}$As layer. The top mirror is the 2D chiral photonic crystal. The propagation of light in this system can be described by the optical scattering matrix. The basic idea is (i) to split the system into several layers in which the dielectric permittivity does not depend on $z$, and (ii) to find the 2D electromagnetic modes of each slab, their electromagnetic field distributions $\{E_x(x,y), E_y(x,y), H_z(x,y), H_y(x,y)\}$, and wavenumbers $K_z$. The periodicity of the structure along $x$ and $y$ axes leads the fields to be represented as products of periodic functions and harmonics $\exp(i(k_x x + k_y y))$, where $k_{x,y}$ are in the 1st BZ, with $-K_{Bz}/2 < k_{x,y} < K_{Bz}/2$.

The $C_4$ symmetry leads the in-plane components of the electric and magnetic fields to be represented after a $90^\circ$ rotation in one of the four forms

$$\{F_x(-y,x), F_y(-y,x)\} = i^n \{F_x(x,y), -F_x(x,y)\}, \quad (5)$$

where $n = -1, 0, 1, 2$, and $F$ means the electric or magnetic fields. The advantages of the periodicity and $C_4$ symmetry can be simultaneously used only for $k_x = k_y = 0$. In this case, the left polarized light

$$E^{-} = E_{x}^{0} e^{-i\omega t} \sqrt{2}$$

propagating in air normal to the structure plane, corresponds to $n = -1$, while the right polarized one corresponds to $n = +1$. Since two other forms are optically inactive (see, e.g., in Ref. [13]), we will consider later only $n = \pm 1$.

3. Time-reversal symmetry

The time-reversal symmetry of Maxwell’s equations for systems consisted of non-absorbing and non-gyrotropic materials relates wavenumbers and electromagnetic fields of the propagating ($\text{Im}K_z = 0$) modes with opposite $n$. If $\mathbf{E}_{3D}(x,y,z)$ and $\mathbf{H}_{3D}(x,y,z)$ are the solutions of Maxwell’s equations for infinitely thick layer, the time-reversal symmetry requires $\mathbf{E}^*_{3D}(x,y,z)$ and $-\mathbf{H}^*_{3D}(x,y,z)$ to be the solutions, too.

Considering the propagation of some mode with fields $\{E_x(x,y), E_y(x,y)\} e^{iK_z z}$ and $\{H_z(x,y), H_y(x,y)\} e^{iK_z z}$, one obtains that $\{E_x^*(x,y), E_y^*(x,y)\} e^{-iK_z z}$ and $-\{H_z^*(x,y), H_y^*(x,y)\} e^{-iK_z z}$ are also solutions. It corresponds to the counter propagating mode with opposite polarization $n$, since complex conjugation of one polarization ($n = +1$ or $-1$) switches the polarization to the opposite one ($n = -1$ or $+1$, respectively). As a result,

$$K_z^+ = K_z^-, E^+ = (E^-)^*, H^+ = (H^-)^*, \quad (6)$$

where the upper indices $\pm$ show the values of $n$. Note that the eigenmodes are always defined up to an arbitrary factor $C$. If propagating eigenmodes are normalized to have fixed energy flow (we choose $\frac{1}{S_0}$ per elementary unit cell), the eigenmodes are still defined up to an arbitrary factor with unitary absolute value $e^{i\omega}$. Hereinafter, we choose the phase $\psi$ for the opposite circular polarizations so that their electromagnetic fields are complex conjugate of each other.

4. Unitary scattering matrix

The optical scattering matrix can be approximately replaced by the unitary scattering matrix $S_{\psi}$ [15]. The thicker the chiral photonic crystal layer is, the better is this approximation. The schematics of the QD emission near the $\lambda_{0,1h} = 910.5$ nm resonance with $n = +1$ or $-1$ (decoupled in case of $C_4$ symmetry) is shown in Fig. 10.

![FIG. 10. (a) Scheme of light scattering in the structure. (b) Schematics of $k = 0$ light emission near the $\lambda = 910.5$ nm resonance. Only the propagating modes are shown, with wavenumbers (in units of $k_0$) $K_{z}^1 = 1$; $K_{z1'} = 2.61, 1.85, 1.32, 1.22$; $K_{s1}$ = 1.11. Actually, there are 12 more propagating modes in the waveguide layer (including the $k = 0, K_z/k_0 = \sqrt{2} = 3.52$ mode), but in comparison with the quasidecoupled mode 1 they do not scatter back from the bottom interface of the waveguide even if they are excited on the top interface and thus can be neglected. Here, $S_{\psi}$ and $S_{\bar{\psi}}$ are the unitary scattering matrixes of the air-CPCS and CPCS-waveguide interfaces, respectively. Hereinafter we omit the subscript $u$ in the scattering matrix notation for simplicity.

In general, the unitary scattering matrix expresses the amplitudes of outgoing modes in terms of the amplitudes of incoming modes:

$$\begin{pmatrix} \text{out}_1 \\ \text{out}_2 \\ \text{out}_3 \\ \vdots \end{pmatrix} = S \begin{pmatrix} \text{in}_1 \\ \text{in}_2 \\ \text{in}_3 \\ \vdots \end{pmatrix} = \begin{pmatrix} r_1 & t_{12} & t_{13} & \cdots \\ t_{21} & r_2 & t_{23} & \cdots \\ t_{31} & t_{32} & r_3 & \cdots \\ \vdots & \vdots & \vdots & \ddots \end{pmatrix} \begin{pmatrix} \text{in}_1 \\ \text{in}_2 \\ \text{in}_3 \\ \vdots \end{pmatrix}. \quad (7)$$

The diagonal elements of the unitary scattering matrix are the reflection amplitudes $r_i$ of the $i$th channel, and
non-diagonal elements are the transition amplitudes \( t_{ij} \) from the \( j \)th channel to the \( i \)th channel.

Similar to the relations in Eq. 6, the time-reversal symmetry of Maxwell’s equations for systems consisting from non-absorbing and non-gyrotropic materials relates also reflection and transition amplitudes in \( \sigma^\pm \) polarizations:

\[
r^\pm_i = r^\mp_i, t^\pm_{ij} = t^\mp_{ji}.
\]

\section{Two-mode resonances}

In the structure of interest, at the resonance wavelength, the QDs excite mode \#1, which leaks along the \( z \) axis primarily through the channels \#1’ and \#2’ with transition amplitudes \( t^\pm_{1\to1'} \) and \( t^\pm_{2\to2'} \), respectively, see Fig. 10b. For both polarizations \( \sigma^+ \) or \( \sigma^- \), these modes propagate through the CPCS with wavenumbers \( K_{z1'} \) and \( K_{z2'} \), respectively. At the top boundary of the CPCS these modes transform into the mode \#1” with the transition amplitudes \( t^\pm_{1\to1''} \) and \( t^\pm_{2\to2''} \), respectively. The total transition probability, including the phase shift due to propagation over the CPCS, is

\[
T^\pm = |t^\pm_{1\to1'} \cdot t^\pm_{1\to1''} e^{iK_{z1'}L} + t^\pm_{2\to2'} \cdot t^\pm_{2\to2''} e^{iK_{z2'}L}|^2,
\]

where \( L \) is the thickness of the CPCS. To simplify the formulas, let’s introduce the new variables

\[
T^\pm_0 = 4| t^\pm_{1\to1'} \cdot t^\pm_{1\to1''}|^2,
\]

\section{Two-mode resonances}

is the oscillating function of the thickness \( L \), which varies from 0 to \( T^\pm_0 \). Moreover, if \( |\varphi^+ - \varphi^-| = \pi \), the transmission in one polarization reaches its maximum when the transmission in the opposite polarization reaches minimum and vice versa. The circular polarization selectivity of transmission \( \rho_{c,T} = (T^+ - T^-)/(T^+ + T^-) \) in these thicknesses appears to be around 100%.

A simple model to estimate the introduced above parameters for the resonance at \( E_0 \) is given in the Appendix. The results of the simplified model are compared with the optical scattering matrix calculation in Fig. 11. Although the parameters of the simplified model seem to differ substantially from the ones calculated within the scattering matrix method with 401 harmonics (see in Tab. 1), the results from this crude model for the circular polarization selectivity of transmission (panel c in Fig. 11) are in a good quantitative agreement with the calculations within the scattering matrix. It happens because \( \eta^\pm, |\varphi^+ - \varphi^-| \) and especially the \( \rho_c \) are sensitive to the ratios of the partial transmissions trough modes 1’ and 2’, which deviate less from the calculated values.

The dependence \( \rho_{c,T}(L) \) is also shown as blue line in panel b of Fig. 11. It can be seen that it is very close to the dependence \( \rho_c(L) \) (green line in the same panel). This fact supports our assumption that it is the selectivity of transmission through the chiral photonic slab that controls the degree of circular polarization of QDs emission in our structure.

\section{Conclusion}

In conclusion, we have fabricated and studied a structure with light emitting InAs QDs inside a GaAs waveguide with a chiral photonic crystal layer on top that demonstrates a strongly circularly polarized photoemission of QDs at zero magnetic field with \( |\rho_c| \) up to 81% and up to 96% if the unpolarized background due to CPCS imperfection is removed. It indicates that the predicted values of \( |\rho_c| \) close to 100% can be reached with further progress in fabrication technology.

The measured angular dependence of the circularly polarized emission intensities near the resonance is shown
to agree with the calculations using the optical scattering matrix. This allows to attribute the circularly polarized resonant emission to the excitation by QDs of the \((\pm2, \pm2)\) Bragg resonance of quasiguided modes in the GaAs waveguide. Based on the reciprocity and symmetry analysis of the structure, we show that the chiral photonic crystal slab in the suggested waveguide structure works as a half-wave plate, exploring the Fabry-Perot interference between the propagating modes in CPCS, to reach nearly a 100% circular polarization of the transmission. The advantage of using the photonic crystal slab with a large contrast of dielectric permittivities is its giant chirality, which allows to fabricate a very thin half-wave plate, with a thickness of the order of the emitted light wavelength. Additional advantage of the CPCS wave plate is its in-plane rotational isotropy, due to the C\(_4\) symmetry.

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Appendix A: Analytical estimation of transition amplitudes

Here we investigate the resonance shown in Fig. [1] in the optimized structure and assume the free space wavelength of light to be fixed and equal to 910.5 nm. The transition amplitudes \(t_{i \rightarrow j}\) in Eqs. [10]–[12] can be roughly estimated via the normalized (see after Eq. [6]) in-plane components of the electric and magnetic fields of modes \(i, j\) as

\[
t_{i \rightarrow j} = \int_{-p/2}^{p/2} \int_{-p/2}^{p/2} dxdy \frac{E_i \times H_j + E_j \times H_i}{2}. \tag{A1}
\]

Here, the symbol \(\times\) means the pseudoscalar product

\[
E \times H = E_x H_y - E_y H_x. \tag{A2}
\]

The CPCS consists of dielectric rectangular pillars that are known to support the waveguide modes (in the vertical direction). The electric (magnetic) field distribution of the waveguide mode with the larger/smaller value of wavenumber \(K_2\) can be roughly approximated by a homogeneous field parallel to the longest/shortest (shortest/longest) side inside the pillar and zero field outside it. Considering four rectangular pillars each rotated by 90° with respect to its nearest neighbors requires the electric and magnetic fields to satisfy Eq. [5]. Note, due to the condition [5], the integral in Eq. [A1] can be taken only over the first quarter of the elementary unit cell (it should be also multiplied by 4), since \(E^*(-y, x) \times H(-y, x) = E^*(x, y) \times H(x, y)\).

The electric and magnetic field distributions of modes \(\#1'\) and \(\#2'\) in the first quarter of the elementary unit cell are

\[
E^\pm_{1'}(x, y) = \begin{cases} \mp iC_1 \varepsilon^{-1/4} e_y, & \text{if } x \in \left(\frac{p}{2}, \frac{3p}{2}\right) \text{ & } y \in (0, \frac{2p}{3}) \text{ otherwise,} \\ 0, & \end{cases} \tag{A3}
\]

\[
H^\pm_{1'}(x, y) = \begin{cases} \pm iC_1 \varepsilon^{1/4} e_x, & \text{if } x \in \left(\frac{p}{2}, \frac{3p}{2}\right) \text{ & } y \in (0, \frac{2p}{3}) \text{ otherwise,} \\ 0, & \end{cases} \tag{A4}
\]

\[
E^\pm_{2'}(x, y) = \begin{cases} C_1 \varepsilon^{-1/4} e_x, & \text{if } x \in \left(\frac{p}{2}, \frac{3p}{2}\right) \text{ & } y \in (0, \frac{2p}{3}) \text{ otherwise,} \\ 0, & \end{cases} \tag{A5}
\]

\[
H^\pm_{2'}(x, y) = \begin{cases} C_1 \varepsilon^{1/4} e_y, & \text{if } x \in \left(\frac{p}{2}, \frac{3p}{2}\right) \text{ & } y \in (0, \frac{2p}{3}) \text{ otherwise,} \\ 0, & \end{cases} \tag{A6}
\]

where the constant \(C_1\) is introduced for brevity,

\[
C_1 = \frac{5}{2\sqrt{2p}}.
\]

The electric and magnetic field distributions of the modes \(#1\) (which is the \((\pm2, \pm2)\) Bragg resonance of the GaAs layer guided mode, in the horizontal direction) and \(#1''\) are

\[
E^\pm_{1}(x, y) = \frac{1}{p} \sqrt{\frac{K_0}{K_{21}}} \left[-\frac{-e_x + e_y}{\sqrt{2}} \cos \left(\frac{4\pi}{p}(x + y)\right) \pm i \frac{e_x + e_y}{\sqrt{2}} \cos \left(\frac{4\pi}{p}(x - y)\right)\right], \tag{A7}
\]

\[
H^\pm_{1}(x, y) = \frac{1}{p} \sqrt{\frac{K_{21}}{K_0}} \left[-\frac{-e_x + e_y}{\sqrt{2}} \cos \left(\frac{4\pi}{p}(x + y)\right) \pm i \frac{e_x + e_y}{\sqrt{2}} \cos \left(\frac{4\pi}{p}(x - y)\right)\right], \tag{A8}
\]

\[
E^\pm_{1''}(x, y) = \frac{1}{p} \frac{e_x \mp ie_y}{\sqrt{2}}, \tag{A9}
\]

\[
H^\pm_{1''}(x, y) = \frac{1}{p} \frac{e_y \pm ie_x}{\sqrt{2}}, \tag{A10}
\]

where the wavenumber is

\[
K_{21} = \sqrt{\frac{\varepsilon k_0^2 - 32\pi^2}{p^2}}, \tag{A11}
\]

\(\varepsilon = 12.42\) is GaAs dielectric permittivity.

Substituting \[(A3)-(A10)\] in \[(A1)\], one can find the transition amplitudes

\[
t^\pm_{1' \rightarrow 1'} = C_2 (C_3 \pm iC_4), \tag{A12}
\]

\[
t^\pm_{1' \rightarrow 2'} = C_2 (C_4 \pm iC_3), \tag{A13}
\]

\[
t^\pm_{1'' \rightarrow 1''} = t^\pm_{2' \rightarrow 1''} = C_5. \tag{A14}
\]
where the constants $C_2$, $C_3$, $C_4$, and $C_5$ are
\[
C_2 = \frac{5}{16\pi^2} \left( e^{1/4} \sqrt{\frac{k_0}{K}} + e^{-1/4} \sqrt{\frac{k_1}{K}} \right), \tag{A15}
\]
\[
C_3 = \sin^2 \frac{\pi}{5}, \tag{A16}
\]
\[
C_4 = \cos \frac{2\pi}{5} + \cos \frac{\pi}{5}, \tag{A17}
\]
\[
C_5 = \frac{1}{5} \left( e^{1/4} + e^{-1/4} \right). \tag{A18}
\]

Substituting formulas (A12)-(A14) into the definitions of $T_0^\pm$, $\eta^\pm$, and $\varphi^\pm$, i.e., Eqs. (10), (11), and (12), respectively, one finds
\[
T_0^+ = C_2^2 C_5^2 (C_4^2 + C_4^2) \approx 0.007, \tag{A19}
\]
\[
\eta^\pm = 1, \tag{A20}
\]
\[
|\varphi^+ - \varphi^-| = \pi - 4\arctan \frac{C_3}{C_4} \approx 111^\circ. \tag{A21}
\]

Thus, as discussed above in Eq. (13) transmission in each polarization depends periodical on the CPCS thickness. As the function of thickness, it varies from 0 to 0.007 and is shifted by 111° with respect to the transmission in the opposite polarization. The comparison of this simple model with the numerical simulation with 401 harmonics is given in the Tab. I. The resulting dependencies of the CPCS transmission in $\sigma^+$ and $\sigma^-$ polarizations and of the circular polarization degree of transmission in comparison with the same formulas (but using exact parameters from Tab. I) and the results of simulation with 401 harmonics are given in Fig. 11. It can be seen that this very approximate and crude model is in a qualitative agreement with the numerical simulations. The dependencies in Fig. 11 calculated with 401 harmonics, demonstrate also sharp peaks, which are due to the influence of other electromagnetic modes in the CPCS, not taken into account in this simple two-mode model. More detail on the comparison of the model with numerical simulations are given in the Supplementary material.

| Variable | Approximate | Simulation | Relative difference |
|----------|-------------|------------|---------------------|
| $T_{\sigma^+}^0$ | -0.0256 + 0.0830i 0.0893 - 0.0073i | -0.0256 + 0.0830i 0.0893 - 0.0073i | 25% |
| $T_{\sigma^-}^0$ | -0.0830 - 0.0256i -0.0147 + 0.0199i | -0.0830 - 0.0256i -0.0147 + 0.0199i | 46% |
| $T_{\sigma^+}^1$ | 0.4820 0.7574 - 0.0063i | 0.4820 0.7574 - 0.0063i | 11% |
| $T_{\sigma^-}^1$ | 0.4820 0.7574 - 0.0063i | 0.4820 0.7574 - 0.0063i | 11% |
| $T_{\sigma^+}^2$ | 0.4820 0.7290 - 0.0561i | 0.4820 0.7290 - 0.0561i | 21% |
| $T_{\sigma^-}^2$ | 0.4820 0.7290 - 0.0561i | 0.4820 0.7290 - 0.0561i | 21% |
| $T_{\sigma^+}^3$ | 0.007 0.0062 | 0.007 0.0062 | 6% |
| $T_{\sigma^-}^3$ | 0.007 0.0075 | 0.007 0.0075 | 4% |
| $\eta^+$ | 1 0.932 | 1 0.932 | 4% |
| $\eta^-$ | 1 0.775 | 1 0.775 | 13% |
| $|\varphi^+ - \varphi^-|$ | 111° 139° | 111° 139° | 11% |

Here, we calculate the relative difference $\delta$ of two variables $a$ and $b$ as $\delta = |a-b|/|a|+|b|$.

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Supplementary material to the manuscript

Controlling circular polarization of light emitted by quantum dots using chiral photonic crystal slab

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The spatial dependences of the scalar product in Eq. (A1) for the approximate $t_{1\to1'}^-, t_{1\to1'}^+, t_{1\to2'}^-, t_{1\to2'}^+$, described in Eqs. (A3-A8), are shown in Figs. 01S, 03S, 05S, 07S, respectively. Figures 02S, 04S, 06S, 08S show the corresponding dependencies, calculated within the optical scattering matrix with 401 harmonics. Left (right) panels show the real (imaginary) parts of the scalar product (A1).

Figures 09S, 10S, 11S, 12S show the in-plane spatial distributions of the electric and magnetic fields of the modes #1, #1', and #2'. See the description of these modes in Subsec.IV.B.5 Two-mode resonances and Appendix A.
Figure 01S. Spatial dependence of the scalar product in Eq. (A1) for the approximate \( t'_{1 \to 1} \). Approximate analytic electric and magnetic fields from Eqs. (A3), (A4), (A7), and (A8).

Figure 02S. Spatial dependence of the scalar product in Eq. (A1) for the approximate \( t'_{1 \to 1} \). Calculated electric and magnetic fields.
Figure 03S. Spatial dependence of the scalar product in Eq. (A1) for the approximate $t_{1}^{+}$. Approximate analytic electric and magnetic fields from Eqs. (A3), (A4), (A7), and (A8).

Figure 04S. Spatial dependence of the scalar product in Eq. (A1) for the approximate $t_{1}^{+}$. Calculated electric and magnetic fields.
**Figure 05S.** Spatial dependence of the scalar product in Eq. (A1) for the approximate $t_{1 \rightarrow 2}'$. Approximate analytic electric and magnetic fields from Eqs. (A5)-(A8).

**Figure 06S.** Spatial dependence of the scalar product in Eq. (A1) for the approximate $t_{1 \rightarrow 2}'$. Calculated electric and magnetic fields.
Figure 07S. Spatial dependence of the scalar product in Eq. (A1) for the approximate $t_{1→2'}^+$. Approximate analytic electric and magnetic fields from Eqs. (A5)-(A8).

Figure 08S. Spatial dependence of the scalar product in Eq. (A1) for the approximate $t_{1→2'}^+$. Calculated electric and magnetic fields.
Figure 09S. Electric (top panels) and magnetic (bottom panels) field distributions of the mode #1 in $n = +1$ (left panels, see also Fig. 10S) and $n = -1$ (right panels) polarizations. See the explanation in Subsec.IV.B.5 Two-mode resonances and Appendix A. In all panels, the blue (red) arrows mark the real (imaginary) part.
Figure 10S. Real (left panels) and imaginary (right panels) parts of electric (top panels) and magnetic (bottom panels) field distributions of the mode #1 in \( n = +1 \) polarization. See the explanation in Subsec.IV.B.5 Two-mode resonances and Appendix A. See also left panels in Fig. 09S.
Figure 11S. Electric (top panels) and magnetic (bottom panels) field distributions of the mode #1' in $n = +1$ (left panels) and $n = -1$ (right panels) polarizations. See the explanation in Subsec.IV.B.5 Two-mode resonances and Appendix A. On all panels, blue vectors mark real part and red vectors mark imaginary part.
Figure 12S. Electric (top panels) and magnetic (bottom panels) field distributions of the mode #2' in $n = +1$ (left panels) and $n = -1$ (right panels) polarizations. See the explanation in Subsec.IV.B.5 Two-mode resonances and Appendix A. On all panels, blue vectors mark real part and red vectors mark imaginary part.