Staged Animation Strategies for Online Dynamic Networks

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Abstract—Dynamic networks—networks that change over time—can be categorized into two types: offline dynamic networks, where all states of the network are known, and online dynamic networks, where only the past states of the network are known. Research on staging animated transitions in dynamic networks has focused more on offline data, where rendering strategies can take into account past and future states of the network. Rendering online dynamic networks is a more challenging problem since it requires a balance between timeliness for monitoring tasks—so that the animations do not lag too far behind the events—and clarity for comprehension tasks—to minimize simultaneous changes that may be difficult to follow. To illustrate the challenges placed by these requirements, we explore three strategies to stage animations for online dynamic networks: time-based, event-based, and a new hybrid approach that we introduce by combining the advantages of the first two. We illustrate the advantages and disadvantages of each strategy in representing low- and high-throughput data and conduct a user study involving monitoring and comprehension of dynamic networks. We also conduct a follow-up, think-aloud study combining monitoring and comprehension with experts in dynamic network visualization. Our findings show that animation staging strategies that emphasize comprehension do better for participant response times and accuracy. However, the notion of “comprehension” is not always clear when it comes to complex changes in highly dynamic networks, requiring some iteration in staging that the hybrid approach affords. Based on our results, we make recommendations for balancing event-based and time-based parameters for our hybrid approach.

Index Terms—Dynamic networks, graph visualization, animation, mental map, user study

1 INTRODUCTION

Within the domain of network analysis and visualization, there is now a growing interest in visualizing dynamic networks: networks that change over time. Visualizing dynamic networks is challenging, as acknowledged by Moody and McFarland [31], who point out “To effectively display the relational structure of a social network, at least two dimensions are needed to represent proximity, and that leaves no effective space (on a printed page) to represent time.” Animation has since been widely recognized as a viable option to show changes to networks that occur over time. However, most techniques introduced to visualize temporal changes in a network are demonstrated on offline dynamic networks, where data is collected and processed offline. Such techniques take advantage of foreknowledge of changes to the network to scale their representations and/or stage any animations appropriately.

On the other hand, visualizing online dynamic network data is challenging since it is generally not possible to predict the future state of the network, or the rate at which new data is generated. It may not even be feasible to identify what behavior to look for, especially if it is previously unseen. Once the behavior is characterized unambiguously, algorithms can be devised to recognize it, but in mission-critical applications, visual display observed by humans is the most practical option to recognize new, unexpected patterns. For instance, security personnel monitor CCTV footage in real time, looking for indicators of threatening events. These “indicators” cannot always be coded to be recognized by an automated system; it depends on the experience and perceptiveness of the person monitoring the footage.

In network visualization, an analogy can be drawn from computer security monitoring, for instance network flow events within the Los Alamos National Laboratory’s (LANL) corporate, internal computer network [31]. These events indicate network connections between computers and contain relevant information such as time of connection, duration of connection, amount of information moved, and the protocol used. Authorized attackers testing network security often create “compromise events” as part of their tests [32]. These events are recorded with information such as domain, source computer, and destination computer. Models are yet to be created to automatically identify some of the compromise events that are recorded in this dataset [32]. Not all malicious behavior recorded in the dataset have validated or correlated indicators. Such events thus need to first be observed and understood manually. Depending on the data sensitivity, real-time visual monitoring could supplement other automated tracking approaches.

Online dynamic network data can be discrete or continuous; i.e., changes to the network can occur either in fits and spurts, or gradually over time [31]. A similar variation can occur with the rate of incoming data as well; i.e., in some instances, a large number of entities (or relations) can appear/disappear over a short time interval, while in other instances there is very little incoming data on entities/relations. A real-time animation strategy can represent these changes with high fidelity—events are shown almost as soon as they occur—but the rate the strategy may fail in providing the viewer with useful information if there are too many changes for the viewer to track.

Alternatively, a staged animation strategy may be devised to keep the user informed of significant changes to the network by “binning” changes until a threshold of time or changes is reached before animating them. However, this strategy has its potential shortcomings: a purely time-based binning may suffer from the same drawback as the real-time strategy when too many changes occur within the fixed time interval. A purely event-based staging strategy addresses the comprehension issue by ensuring that the user does not get overwhelmed by changes to the network in a single stage. This could mean that the animation staging and the duration of the animation for each stage could cause a bottleneck, increasing the time lag between the event occurring and when it is shown to the user. In addition, this could also result in long wait times between updates for low data rates. Staged animation strategies have the added requirement of devising means to inform the users about the cause behind re-organizations to the network [33], which may be implicitly apparent in a real-time strategy. Any animation technique developed to visualize online dynamic networks thus needs to address both requirements: provide the viewer with timely and understandable “chunks” of information on both what changes have occurred to the network and/or layout and why, without significantly compromising the time lag between events and their on-screen depictions.

In this paper, we compare time-based and event-based staging strategies, along with an alternative, “hybrid” staging strategy that we introduce. The hybrid staging strategy uses a combination of time-based and event-based staging, whichever threshold is reached earlier. We motivate each strategy by examining the requirements of animations when it comes to monitoring and comprehending dynamic networks. We evaluate all three strategies through a within-subjects study with 21 participants who perform a series of monitoring and comprehension tasks with each animation staging strategy. A comparison of task
A comprehensive review of dynamic network visualization techniques is provided by Beck et al. [5], who categorize the techniques into animation or "time-to-time mapping", timeline or "time-to-space mapping", and hybrids of both approaches. In this section, we will briefly cover all three techniques with a greater emphasis on time-to-time mapping given the scope of our paper. We will also examine differences between offline and online dynamic networks and the challenges presented by the latter, and go over some basic principles of animation that inform our exploration of the design space we consider for our study.

2 Related Work

A comprehensive review of dynamic network visualization techniques is provided by Beck et al. [5], who categorize the techniques into animation or “time-to-time mapping”, timeline or “time-to-space mapping”, and hybrids of both approaches. In this section, we will briefly cover all three techniques with a greater emphasis on time-to-time mapping given the scope of our paper. We will also examine differences between offline and online dynamic networks and the challenges presented by the latter, and go over some basic principles of animation that inform our exploration of the design space we consider for our study.

2.1 Static Representations of Dynamic Networks

The challenge in visualizing dynamic networks lies in accurately depicting the changes that occur to the network over time, while also ensuring that salient changes are perceptually more apparent to the user. Timeline-based approaches achieve this by providing an overview of changes that occur between time steps. For instance, TimeArcTrees, a technique introduced by Greilich et al. [27], vertically aligns graph nodes across time steps, facilitating comparison between two states based on position of the nodes and the organization of edges between nodes. While graph scale is somewhat addressed by collapsing subgraphs into parent nodes, comparison between two graphs still requires a one-to-one comparison between nodes. Burch et al. [9] address this issue in TimeArcTrees by introducing parallel edge splatting: each time-state of the graph is first mapped to a 1D vertical layout, with edge overplotting and weighting shown as a heatmap between parallel lines. Reda et al. [41] address issues of scale by focusing on communities: each entity in the network is plotted as a polyline extending from left to right, with vertical movements of the polyline corresponding to its membership in the communities that exist within the time period of interest. Polylines that stay in the same community over time are bundled together to form a band, further addressing issues of scale. Vehlow et al. [27] improve on this work by using Gestalt principles to show continuity between communities as they merge or split over time, and use color to depict similarities between communities over time. Though timeline-based representations actively focus on the issue of scale, they are restricted to a finite screen space in which to show all salient states of the graph. Previous works [41,45] have used a model for dynamic graphs which is not based on time slices using the DynNoSlice force-directed algorithm which uses a space-time cube (2D+time) to visualize an offline dynamic graph. Static representations of dynamic graphs have been shown to work better than dynamic representations for analysis [6,18,44,45] but such representations are more suitable for offline dynamic graphs, where the states of the network are known in advance. Real-time data would produce a larger number of static states as each event can be considered a new state without periodical summarising or binning of the states.

2.2 Animated Representations of Dynamic Networks

In contrast, animation-based techniques—typically based on node-link diagrams—offer a more intuitive visualization of dynamic networks. Force-directed layout generation is one of the most common approaches for visualizing networks. The method produces aesthetically-appealing layouts for static networks, but is also useful in visualizing dynamic networks as changes to the network—modeled as particles entering/leaving the system and coupling with/decoupling from other particles in the system—can result in smooth animations. However, force-directed approaches are not without fault: minor changes to the graph, such as the linking of two disconnected components, can have a large impact on the overall layout. Because position is used to encode entity relations, a user can form and maintain an abstract interpretation of the network’s structure, called a “mental map” [13]. In their review of dynamic graph visualizations, Beck et al. [5] identify the main goal of animation-based techniques to be the preservation of this mental map, typically by keeping the position of nodes in node-link diagrams stable over time, thus minimizing the visual difference between the layouts of the network across different time slices.

2.2.1 Animated Transitions in Offline Dynamic Networks

Most strategies for computing transitions between dynamic network states have been developed for “offline” dynamic graphs, whose structure over time is known at the time of visualization [5]. Computing strategies thus use this ability to “look ahead” and anticipate changes that inform the current layout. For instance, Diehl and Görg [13] introduced a metric called “mental distance” to indicate the similarity between two layouts, and built a metagraph from the time sequence to help preserve the mental map. They also introduced a Foresighted Layout with Tolerance (FLT) approach for force-directed graphs that trades layout quality of individual graphs for overall graph stability to preserve the mental map. Görg et al. [25] extended FLT to hierarchical and orthogonal layouts and developed adjustment strategies for each. Initial approaches to lay out dynamic graphs used the GRIP algorithm [23] for its speed in laying out large graphs. For instance, Collberg et al. [11] added time-slice information to the GRIP algorithm to compute distances between corresponding nodes from consecutive time slices of the same graph. A similar approach was used by Erten et al. [17] who modified GRIP to preserve the mental map by minimizing positional changes between nodes in one timeslice to the corresponding nodes in subsequent timeslices. Brandes et al. [7] argue for the suitability of spectral layouts to visualize dynamic networks, as layout changes scale proportionally to changes in the graph. They demonstrate their argument using spectral methods to animate small-world network models over time. More recently, GraphDiaries [4] combines the advantages of timeline and animated approaches to represent dynamic graphs. It uses small multiples to provide an overview of the network states over time, and uses staged animation transition to show the user what changes between two given states.

When visualizing large dynamic networks, it becomes infeasible to track individual node positions, and approaches focus instead on tracking clusters. Kumar and Garland [35], for instance, propose a stratification technique to visualize hierarchies in large graphs, and extend their approach to dynamic networks by tracking the changes in the clustering metric over time and minimizing changes in node positions. A similar technique of clustering nodes that share a common motion from initial layout to the target layout is mentioned in [20]. Sallaberry et al. [42] use their previous rapid graph layout approach [38] to compute clusters in a given dynamic network at each time step, and use supporting views to visualize how clusters evolve over time.

2.2.2 Animated Transitions in Online Dynamic Networks

The main challenge for online dynamic networks is that visualization strategies can only take into account the past states of the network as the future states are unknown. Unknown future states of a network can result from the data itself, with the addition or removal of new entities and/or relationships. They can also result from user interactions, such as filtering or reorganizing data. In both cases, the objective remains the same—preserving the user’s mental map of the network—while the challenges are different. Most prior work on visualizing online dynamic networks address changes due to user interactions rather than changes due to streaming data. Early approaches to address the inherent unpredictability of these networks used random field modeling where models of the layout and its stability were used by a stochastic estimator
that computes layouts in terms of random fields [8], but ignored mental maps when computing the layouts. Brandes et al. [7] whose spectral layout is discussed in Section 2.1 argue that their approach can be applicable to online dynamic networks, as it is based on the assumption that since the graphs in consecutive time steps are similar, spectral layouts of these graphs do not vary significantly.

However, there has been some work done on online graphs that involve “streaming” data. In early work, North [19] proposed a heuristic called DynaDAG for directed acyclic graphs to view incremental updates to graph layouts based on a combination of operational primitives. Lee et al. [25] used simulated annealing to address the challenge of preserving the mental map while addressing changes in the network from streaming data, but at the cost of speed as the approach redraws the entire layout at each time step. Frishman and Tal [21] introduce “space vertices” that minimize the movement of graph clusters between successive layouts as a technique to preserve the mental map between updates. In a later work [22], they address the same problem by proposing an algorithm that uses a pinning weight to identify computationally-intensive parts of the network, i.e., areas of the network that change over time, and computes their layouts using the GPU. Gorochowski et al. [26] suggest a similar approach: an “age-directed layout” technique where both colors and adjusts the degree of a node’s movement based on its “age”. Nodes that show fewer updates to their connections over time are considered “older” and move less, whereas “younger” nodes are subject to greater movement. Hayashi et al. [29] use two techniques to manage changes to the graph: an automatic edge resizing technique reduces variations in edge lengths over time, while a sorted sequential barycenter merging technique updates the graph with new nodes based on their connectivity to the existing nodes. Both techniques reduce variation in the graph to preserve the mental map.

In more recent work, Cnavosvan et al. [12] use an incremental algorithm based on FM [24], which uses GPU acceleration for fast computation. The incremental algorithm, which enables fast computation between updates while preserving the mental map, is followed by a refinement technique that uses an energy-minimization strategy to reduce edge crossings and lengths for an aesthetic layout. In our study of staging strategies, we use this incremental algorithm to preserve the mental map and refine the graph layout between animation stages.

2.3 Staged Animation and Perception

In the prior sections we looked at static and animated representations of dynamic networks. While static representations can provide an excellent overview, animation provides a metaphor for transition (in the form of movement) consistent with our mental model of the physical world. In addition, animations can convey not only transitions, but also causality [23] (e.g. move nodes apart after deleting an edge between them). Animated transitions are widely used in human-computer interaction (HCI) for providing fluid interactions and in information visualizations to maintain continuity between different states of visualizations [16].

While layout strategies optimize the use of space—specifically, the use of displacement—to preserve mental maps, animations can be said to use time for the same purpose. However, animation needs to be used with care. When animations show complex interactions of moving parts, the viewer’s perception of transitions may be inaccurate [46]. Moreover, there are perceptual limits to the number of independently-moving objects our visual attention can simultaneously track [49]. This ability is further impacted by the speed of the animation; faster animations reduce the number of objects we can track simultaneously, while also reducing the tracking accuracy [19]. Strategies to minimize the number of “objects” that the user needs to track typically discretize objects over time and/or space. Trajectory bundling, for instance, uses discretization over space, “grouping” individual objects and moving them together, thus taking advantage of the Gestalt principle of common fate to improve the viewer’s ability to track more points [4]. On the other hand, staged animation [30] uses the discretization-over-time approach, where animated transitions are presented in stages over successive time intervals. While users consistently prefer staged animations over simultaneous ones, it is not always recommended. Staging can increase the time span between events, rendering the user’s short-term memory unreliable [4].

When it comes to dynamic graph visualization, there is a limit to the amount of trajectory bundling that can be done while preserving the mental map of the graph, making staged transition a promising strategy. GraphDiaries [43] is the only work that, to our knowledge, examines strategies in staging animations in dynamic graph visualization. They split the staging into element removal, transformation and addition in that order. This order is shown to be optimal in reducing ambiguity while also minimizing transition time. However, GraphDiaries is designed for offline dynamic graphs, allowing for the choice of staging strategies ahead of time to reduce the user’s perceptual load. Wang et al. [48] investigate a non-uniform time slicing approach by adapting histogram equalization to create time slices of equal visual complexity, thus conveying more important details of time slices when there is a sudden influx of edges. However, due to the lack of user studies, it remains unclear which graph analysis task benefits from the non-uniform and uniform time slicing approach.

In this paper, we explore animation strategies for online dynamic graphs, wherein we adapt staging order and timing from GraphDiaries but study the effects of time-based and event-based animations, as well as a hybrid of the two approaches that we introduce.

3 DESIGN CONSIDERATIONS

Analyzing changes to dynamic networks in real time involves two main kinds of tasks: monitoring, where the analyst needs to become aware of a particular kind of change as soon as it occurs, and comprehension where the analyst needs to understand what changes have occurred to a graph over a period of time. For real-time analysis, it is safe to assume that this period of time is relatively short. From the related research, it is clear that there are several tradeoffs that need to be made in order for the viewer to keep track of the changes. The balance lies between keeping the analyst aware of changes to the network as soon as they occur, yet not overwhelming them with too many updates to the network. We posit that the design of staged animated representations of change in online dynamic graphs needs to balance three aspects:

R1 Timeliness: The animated representation of the event should occur as close as possible to the actual time of the event.

R2 Mental Map preservation: The animated representation should occur in a way that allows the viewer to track the changes to the graph, thus preserving their mental map of the graph.

R3 Minimize Transition Time: The animated transition should be short enough to make effective use of the viewer’s short-term memory in recalling the changes in the graph.

For the purpose of this paper, we focus on changes to the network that are triggered by new data, rather than by user interactions. We use Chevalier et al.’s definitions of transition and animation [10] to define the design space of staged transitions. They define transition as a pair of visual states (initial and final). An animation is a series of images that provides the impression of perceptual continuity between the initial state of the transition and the final state. We also define, for the purpose of our study, an event as a change in the network. An event can thus be (a) the appearance of a new node, (b) the appearance of a new edge, (c) the disappearance of an existing node, (d) the disappearance of an existing edge, and (e) a combination of (a) and (b) or of (c) and (d). We define a stage of the animation as a representation of one or more events collected based on a triggering parameter. Since events occur over time, we consider both time intervals and event count as triggering parameters for these stages. Finally, we define animation time as the duration over which the animation plays out on the interface.

We base our animation design itself on Bach et al. [4], who report that while deletion of nodes/edges and addition of nodes/edges may both trigger positional changes to the network, pre-computing these and ordering them as deletion-movement-addition works best to preserve the viewer’s mental map. Our animation time $T_{an}$ will thus also be split into a time $T_{f}$ over which entities are deleted, time $T_{m}$ over which they are moved, and a time $T_{p}$ over which new entities are added, in that order (see bottom right of Fig. 1). In addition, we include a “pause time” ($T_{p}$) after each animation to perceptually distinguish one stage.
From another. Without a pause, the user would perceive a continuous series of animations instead of the intended stages. Thus, the total animation time \( T_{an} = t_d + t_m + t_a + t_p \) as seen in Fig. 1. Based on this, and on the requirements above, we examine three strategies of staged animations. For our study, we set \( t_d = 450\,\text{ms}, t_m = 600\,\text{ms}, t_a=450\,\text{ms}, \) and \( t_p=500\,\text{ms} \), for a total animation time of \( T_{an} \) of 2 seconds.

**Time-based staging:** As the name implies, this staging strategy uses a specified set of time intervals \( t_i \geq t_2 \) over which events are recorded. Events are separated into deletions and additions, and the new positions of the nodes in the dynamic graph are computed. At the end of this time interval, the animation renders deletions, movement to new positions, and additions in sequence. This process is repeated for successive time intervals \( t_i \). One of the main advantages is that regardless of the data influx, the animation will lag behind the actual events by a maximum of \( t_i + t_m \), satisfying the timeliness requirement (R1). However, this strategy does not place an upper limit on the number of events per animation stage. For instance, Fig. 1(a) shows three stages of animation, with 4, 6, and 3 events respectively if represented using time-based staging. For high data influx, the number of events per stage can grow to an overwhelming proportion. Since there is no way of predicting the data influx for online dynamic network, the effectiveness of this staging strategy hinges on the data influx rate and the choice of \( t_i \). The time-based staging strategy is thus more suitable for monitoring rather than comprehension tasks, provided the animations are not overwhelming. For the purpose of our study, we use 2 seconds as the value of \( t_i \).

**Event-based staging:** Given that human visual perception is limited in terms of the number of independently-moving objects it can track, it is reasonable to explore an animation staging strategy that counts events as they occur, and deploy the events once a threshold of \( N \) events has been reached. The separation of events and the subsequent animation follows the same process as time-based staging, but there are a few differences in the staging of the animation. The number of events shown per stage is limited, which helps with comprehension and mental map preservation (R2). However, even when the data influx rate is high, only \( N \) events can be shown for every time period \( T_{an} \), the animation time. If the number of events that occur over \( T_{an} \) is greater than \( N \), it results in events “piling up” to be animated, resulting in an increasing time lag between the event and its animation. On the other hand, when the data influx rate is very low, such as when the time taken for \( N \) events to occur is much higher than \( T_{an} \), those events are not shown at all until the event threshold is reached. Fig. 1(b) illustrates this issue. While three events have occurred after Stage 2, they are not shown to the viewer as the event threshold is \( N = 5 \) in this example. Both these conditions illustrate how an event-based staging strategy does not satisfy the timeliness requirement (R1). Event-based staging strategies are thus more suitable for comprehension tasks rather than those involving monitoring. In our study, we use \( N = 5 \) for comprehension tasks and \( N = 3 \) for monitoring tasks.

**Hybrid staging:** In order to address the shortcomings of time-based and event-based staging strategies, we introduce a combination of the two: a hybrid strategy that uses both event and time thresholds to trigger the next stage of the animation. Thus the animation triggers at a specified event count \( N \) or at a specified time interval \( t_i \), whichever occurs earlier. For high data influx, the staging is based on an event-based trigger, prioritizing comprehension (R2) over timeliness. For low data influx, the staging is based on a time-based trigger, prioritizing timeliness (R1). Comprehension is not compromised in this case as the data influx rate is low. Traditional event- and time-based animations use uniform timings, even when there are no addition or deletion events. This uniformity helps reduce mental load on the user as they can anticipate events. However, when no events occur, this can contribute to the animation “lag”. Since our goal with the hybrid staging was to reduce lag without compromising comprehension, we use a variable animation time based on the kinds of events recorded for each stage. Thus, if there are no deletion events in a stage, the animation time reduces to \( T_{an} = t_m + t_a + t_p \). Alternately if there are no addition events, the animation time reduces to \( T_{an} = t_d + t_m + t_p \). There can also be cases where the time threshold \( t_i \) is reached with no events occurring, and this can trigger a convergence of the graph involving only movement. In this case, the animation time is simply \( T_{an} = t_m + t_p \). This reduces the transition time overall, making more effective use of the viewer’s short-term memory (R3). The hybrid staging strategy thus combines the advantages of both time-based and event-based strategies, except in the case of high-throughput data, where its timeliness is equivalent to that of the event-based strategy. However, the introduction of variable animation time reduces unnecessary time delays even in this situation. For our study, we maintain the same event and time thresholds for the hybrid staging as we do for event- and time-based staging.

We implement all three approaches for our user study in order to compare these three strategies for both monitoring and comprehension tasks in online dynamic networks.

**4 IMPLEMENTATION**

Given the focus of our study on monitoring and comprehension, our implementation of staged animation of online dynamic graphs precludes any user interaction with the system. This is an artificial constraint as most visualization or visual analytic systems for monitoring networks would have some control for overview, filtering and playback. Yet, it was necessary for our controlled study to exclude other variables that
Fig. 2. Illustration of how the staged animation appears to the participants in the study, inspired by GraphDiaries [4]. At the start of the deletion stage, all entities (nodes/edges) to be deleted flash orange, and then disappear over the next 0.5 seconds. Labels of deleted nodes remain briefly for the participants to register what entities have disappeared. The remaining nodes move (1.2 sec) to their new computed positions. Entities that are added flash blue briefly and the color fades away (0.5 sec).

might influence the perception of the results from each staging strategy. Our implementation thus focused on only one aspect, graph layout, other than the staging strategies.

A crucial aspect of dynamic graph layouts is how each time step is laid out. In offline dynamic graph layouts, a trade off is made between globally optimized layout for all times or local optimized for each time. Since online dynamic graph layouts do not posses the knowledge of all the time steps ahead of time they focus on reducing the amount of movement nodes experience between each time point. We utilize the incremental layout method work by Crnovrsanin et al. [12]. Their qualitative study demonstrated improved results over the two other state-of-the-art methods: Aging [25] and Pinning [22]. Their methods consist of two parts, an initial placement and layout algorithm followed by a refinement approach. The refinement allows nodes with high energy to move until they reach a low energy state. Due to how staged animation works and for the study, we had to make a few changes to how their layout method operates. In their implementation, refinement is run between time steps while the system waits for more data.

The benefit of this approach is that it allows a gradual change of the network and helps to maintain the stability of the network over time. The incremental layout method that we use [12] has two options: either refine the layout gradually between the time steps, or perform refinement and layout out the graph without showing the intermediate steps. Unfortunately, in our implementation, we cannot run refinement between time steps due to constant data coming in the study. Therefore, we run refinement right after the initial placement of new nodes and edges, followed by the layout algorithm but before staged animation is run. This gives the movement from both the addition and deletions as well as high energy nodes shifting to a low energy state. Another change is an addition of a central force for all nodes to keep them closer to each other. Without this central force, disconnected components would continue to move away over time. A side benefit is this allows us to fit all nodes within the screen, making it easier to conduct the study. The actual disappearance, movement, and appearance of the entities in each stage follows GraphDiaries [4] closely (see Fig. 2).

Fig. 3. Chart showing the rate at which the events occur over time in the raw data (left), and the number of nodes at the start and end of the animation for each task (right). The duration over which these events are displayed in the animations will depend on the animation strategy used.

5.1 Participants
We recruited 21 participants (9 female, 12 male) between 18 and 35 years of age. All participants were university students, with 12 Ph.D students, 6 masters students, and 3 undergraduate students. Eighteen students were computer science majors, the remaining three majored in Aerospace engineering, Telecommunication, and Information Technology, respectively. Most of the participants (13 students) reported being highly familiar with information visualization. Five were moderately familiar with visualization, while three had little to no familiarity with the subject. Eight of the 21 participants reported using node-link diagrams regularly in their work, an equal number reported having used them at least once, while the remaining 5 had little or no knowledge of node-link diagrams.

5.2 Apparatus
Of the 21 participants, 16 used a MacBook Pro laptop with a 2.7 GHz Intel Core i5 processor and 8 GB RAM, connected to a 30 in display (2560 x 1600 resolution). Due to logistical constraints, five participants participated remotely, and used different monitors (all 15-inch laptop screens). All animations were shown to participants as video clips with no playback controls. The questionnaire including video playback was administered on a Chrome browser.

5.3 Tasks & Dataset
In order to generate the animations illustrating the three staging strategies, we used the MIT Reality Mining Dataset [15]. The dataset contains activity records of 100 individuals at MIT over the span of the 2004-2005 academic year and includes datasets recording proximity, location, communication, and other activity. In this study, we draw from subsets of this data concerning the activities labelled Call and Proximity. The Call dataset contains temporal data of individuals placing calls to others, while the Proximity dataset contains temporal data of individuals moving in and out of each other’s Bluetooth ranges. For our tasks, we choose temporal data segments from different sections of the larger dataset. This allows us to choose segments with variations in the rate at which events occurred over time (see Fig. 3). In addition, the two types of networks present in the data set (call and proximity) are structurally different from each other.

As mentioned earlier, tasks were split into monitoring and comprehension tasks. Monitoring tasks were timed. The question was asked before the video was shown to the participants, and they needed to respond during the video playback as soon as they spotted the answer to their question. Participant response times were noted relative to when the event occurred, in addition to when the event was shown in the animation (see Fig. 4 for details). Comprehension tasks were multiple-choice, and required participants to observe a video and then answer one or more questions related to the video. We used node labels for tasks that required paying attention to specific nodes, and kept the nodes unlabeled for tasks that were more general, e.g. paying attention to clusters or the overall graph. Table 1 describes the tasks used in the study. A third comprehension task was initially included in the study but subsequently dropped from the analysis due to the fact that the event-based and hybrid staging resulted in identical “batches” of animations, with only the node positioning being different. This would have created an unintended confound.

5 User Study
Our goal through the user study is to determine the suitability of each staging strategy to a number of tasks broadly based on task taxonomies for network visualizations with temporal components [12, 23]. We broadly split our tasks into monitoring and comprehension tasks, or elementary and synoptic tasks respectively, according to the Andrienko Task Format (ATF) [2]. We designed a within-subjects study where each participant was exposed to multiple monitoring and comprehension tasks using all three animation strategies. We supplement this study with a follow-up qualitative study with two experts in network visualization (see Sect. 7). We use a think-aloud protocol to evaluate their comprehension of a set of online dynamic network animation videos across the three animation strategies.
Under Koussoulakou and Kraak’s classification of spatio-temporal tasks [34], the monitoring tasks can be categorized as elementary under space and intermediate under time, as participants are typically tracking one or two nodes over a given duration, looking for a specific behavior. The comprehension tasks in this study as well as the follow-up think-aloud study fall under “overall level” under both space and time in the same classification, as participants are asked to report on the overall behavior of a node, group of nodes, or the entire network over a time duration. In terms of tasks specific to network visualization, we use as reference Ahn et al.’s taxonomy [1], where temporal features are broadly classified into individual temporal features that are typically event-related, shape of changes that concern event collections such as growth/contraction, stability etc. and rate of changes that involve the measurement of speed or time. Since ours is an exercise in perception and not measurement, our tasks do not fall under the rate of changes category. Using this classification, our monitoring tasks can be categorized under individual temporal features, while the comprehension tasks and the think-aloud tasks in the follow-up study can be categorized under shape of changes. Participants were given training questions for each type of task: one question for monitoring, and two for comprehension.

| Task Type | ID | Task Description |
|-----------|----|------------------|
| Monitoring | T1 | Track clusters and respond as soon as they merge. |
|           | T2 | Track graph and respond as soon as a particular named entity (node) appears. |
|           | T3 | Track graph and respond as soon as two named entities (nodes) are linked. |
|           | T4 | Entity pointed out before the video, and after the video playback, asked what happened to it over the course of the animation. |
| Comprehension | T5 | Cluster pointed out before the video, and after the video playback, asked what happened to it over the course of the animation. |

Table 1. Task categorization and description for each staging strategy

In real-world applications such as our security networks example, the individuals who monitor the networks are intimately familiar with said network. Based their knowledge of prior attacks, they can judge which nodes are vulnerable and need attention. While it would be difficult to (a) find a suitable number of network security experts and (b) set up the data to suit their prior knowledge of similar networks, we were able to simulate this prior knowledge by asking participants to pay attention to certain nodes.

In addition, real-world scenarios would likely have additional embellishments such as highlighting on recently-changed portions of the network visualization. However, we decided to use it sparingly for a number of reasons. Given our focus on understanding which staging strategies best use participants’ capabilities to discern changes in networks, we use highlighting as shown in Fig. 2 to draw attention to node creation and removal. Other forms of highlighting that draw attention to certain categories of behavior often do so for the user to step back in time and review what happened to the highlighted nodes. This would make sense in a long-term case study of an actual network being monitored, but not in our controlled study.

Since most participants were not expected to be familiar with dynamic graphs and node-link diagrams, the questions were mostly phrased in the context of a social network. For instance, T3 was worded as “You will be shown a friendship network with users shown as nodes and relationships between them shown as edges. Look out for Ryan and Emily, and click on the button as soon as they become friends.” This being a full-factorial within-subjects design, tasks T1–T5 were repeated for each condition, i.e. each animation staging strategy. We used the same dataset for each condition, with labels changed and graphs rotated/mirrored for each condition. While the graphs were all identical (except for rotation/mirroring) at the start of the animation, the different staging strategies would result in changes in layout between the three staging conditions. While this potentially introduces an additional variable (layout) into our study, it is unavoidable within the scope of this work. All tasks were performed in sequence (T1–T5) for each condition. We counterbalanced the condition order using a Latin Square design to mitigate learning effects.

5.4 Procedure

Individual participants were first given a basic background of the study, but were not described the specific animation techniques, so as to not bias them. Instead, they were told that data would be shown to them in three different forms, and that they would be asked to perform a set of tasks for each form of data presentation. All questions and tasks were presented in the form of an online survey, with the video showing animations embedded in the survey. To ensure participants see the video only once, playback controls were disabled. Due to the animation strategies used, the video durations varied for each condition. Table 2 shows video duration for each task and condition.

| Task ID | Video duration (sec) |
|--------|----------------------|
| T1     | 34 34 16 |
| T2     | 75 65 23 |
| T3     | 108 96 15 |
| T4     | 69 65 28 |
| T5     | 92 75 37 |

Table 2. Video durations for each task and staging strategy. Note that the data shown is the same for each task; the varying durations are a result of the staging strategies. Note that for T1–T3 (monitoring), participants are not required to watch the entire video.

In the case of monitoring tasks, the video was accompanied by a button labelled “Click as soon as you find (the answer)”, and the time elapsed between the start of video playback and the button click was recorded. Note that for monitoring tasks, participants do not have to watch the entire video. Participants were presented with all 5 tasks in the same order for each condition (animated staging strategy). Our study thus involved 21 participants × 3 staging strategies × 5 tasks, resulting in a total of 315 trials. At the end of each condition, participants also filled out a NASA Task Load Index (TLX) response sheet [25]. Note that we collected the NASA TLX data once per condition rather than once per task to avoid survey fatigue. A typical session lasted 45 minutes.

5.5 Hypotheses

Based on our design considerations and the requirements outlined in Section 3 we formulated the following hypotheses:

H1 Participant response to the monitoring tasks will be affected by the volume of data. They will be quicker for event-based staging conditions than the remaining two as the reduced visual complexity would help them spot the event as soon as it happens. For the same reason, we posit that hybrid staging will prompt quicker responses than time-based staging. Response time is a stand-in for the ability to perceive an event that occurred.

H2a Participant responses to comprehension tasks will show more errors in time-based staging conditions than the remaining two due to the increased visual complexity to which time-based staging is susceptible given a high rate of data influx.

H2b Participant responses to comprehension tasks will show more errors in event-based staging conditions than in hybrid staging conditions due to the greater time period for which participants need to track and remember events.

H3a Participants will report lower levels of performance and higher levels of frustration in time-based staging conditions when compared to the remaining two.

H3b Participants will report higher levels of mental, physical, and temporal load and effort in time-based staging strategies when compared to the remaining two.

6 Results

We split our results into monitoring (hypothesis H1), comprehension (H2a & H2b), and participant experience (H3a & H3b), and report the results in detail under each.
6.1 Monitoring Tasks

Fig. 4 shows participant response distribution for monitoring tasks (T1–T3). The figure shows two kinds of delays: (1) the delay in participant response when compared to the actual event (the boxplots in the figure) and (2) the delay between an event occurring and it being shown in the video (the horizontal black lines in the figure). We separate the two delays. We measure the difference between the time at which the participant is shown the event and the corresponding response as the “participant response time”. We use this as a measure of how easily the participant was able to see the event when it was shown to occur (hypothesis H1). This also addresses cases where participants respond before the event occurs, which in monitoring tasks is an error at the same level or worse than a delayed response. We observe in the raw data that this happened only for three participants in time-based staging.

We analyzed the participant response times using a repeated-measures analysis of variance (RM-ANOVA) and found a significant effect of animation staging strategy on the time difference between participant response time and the time at which the event was shown on the video for tasks T1 ($\chi^2 = 15.89, p < 0.001$), physical demand ($\chi^2 = 8.79, p < 0.05$), temporal demand ($\chi^2 = 9.66, p < 0.01$), effort ($\chi^2 = 5.05, p < 0.001$), and frustration ($\chi^2 = 11.14, p < 0.01$). No significant difference was found for participant responses on performance. A posthoc Conover test revealed pairwise significant differences (see Table 3).

From the table, we see that participants were significantly more frustrated using time-based staging than the other two, though participant self-report of performance showed no significant differences (partially confirming H3a). On the other hand, mental load, physical load, temporal load, and effort were all significantly higher for time-based staging than for the remaining two (confirming H3b). In fact, with the exception of mental load, there are significant differences in participant perception of load, effort, and frustration between hybrid and event-based strategies as well, with hybrid performing better than event in terms of temporal load and worse in the other measures.

6.2 Comprehension Tasks

Fig. 5 shows the distribution of correct and incorrect answers for all the comprehension tasks, categorized by animation staging strategy.

6.3 Participant Experience

The distribution of participant responses on the NASA TLX for each staging condition is shown in Fig. 6. We performed Friedman’s test on each scale separately, and found significant differences between the staging conditions for participant responses on mental demand

| Task | Condition | Score (median) | Tukey HSD Significance |
|------|-----------|---------------|------------------------|
| Mental | Event | 9 | – | ** |
| | Hybrid | 10 | – | ** |
| | Time | 15 | ** | – |
| Physical | Event | 3 | – | ** |
| | Hybrid | 3 | – | ** |
| | Time | 4 | ** | – |
| Temporal | Event | 9 | – | ** |
| | Hybrid | 7 | – | ** |
| | Time | 11 | ** | – |
| Effort | Event | 10 | – | ** |
| | Hybrid | 10 | – | ** |
| | Time | 13 | ** | – |
| Frustration | Event | 5 | – | ** |
| | Hybrid | 6 | – | ** |
| | Time | 11 | ** | – |

Table 4. Participant responses on the NASA Task Load Index for each condition with pairwise significant differences marked.
7 Follow-Up Study with Experts

The participants in the prior study did not have much expertise in network visualization, though they had varying degrees of familiarity with the subject. To follow up on our findings with observations from expert participants, we conducted a qualitative study of the three animation strategies with domain experts in network theory and visualization. The participants (P1 and P2) were Graduate Ph.D. students with over 5 years of experience in network analysis and visualization, and they design and implement new network visualization techniques.

We followed a think-aloud protocol where each participant was shown an animation of a dynamic network, and asked to narrate aloud what they thought was happening throughout the animation. At the end of each animation, they were asked follow-up questions on what they had just observed, and about the state of the network in general, and observations they had made in particular. The video was played only once (during the think-aloud component), and participants were asked not to play back the video. The study was administered remotely via web conference, with both participants using Mac Book Pro laptops with resolutions of 2560 × 1600 and 1920 × 1080 each.

The study involved 3 different animation clips for each animation strategy. One clip used the MIT proximity dataset [31] mentioned in Sect. 5.3 while the remaining two clips used the LANL dataset mentioned in the introduction. For the MIT dataset, participants were asked to observe and track individuals that moved through the network the most, and individuals who had high centrality, i.e. those who connected two or more clusters of the network. For the LANL dataset, participants were asked to keep track of computers that connected to multiple other computers, and those that switched connections between different computers frequently. Participants viewed training clips to familiarize them with the kind of data they would observe and their contexts. They were shown video snippets describing what behaviors in the network we are trying to identify. For example, we showed the users video snippets of what a stable network would be. As in the previous study, the same data was animated using the three different strategies and shown to the participants. Learning effects were minimized by (a) ordering the clips so that the same data was not shown in successive clips, and (b) changing the node identifiers between animation strategies. Finally, the order in which the videos were shown were switched up between participants. Our observations are described below.

Time-Based Animation. Participants’ responses to time-based animation clips seemed rushed. They were unable to follow sudden changes that occurred in the network, and found it difficult to track individual node connections. To catch up to the rapid changes in the network, the participants went from using specific network terminologies to describe changes to general phrases such as “I see a lot of changes in the network” (P1), and “changes happening everywhere” (P2). However, we noticed that both participants provided similar descriptions of the overall network evolution, especially attributes such as changes in network size and stability of clusters.

Event-Based Animation. Participants found certain sections of the network to be quite dense, stating that they seemed like a “hairball” which made it difficult to identify which nodes were connected to which others. The participants were able to identify the overall network evolution trend which included descriptions of stability and cluster changes. There were sections of the video where both the participants claimed to seeing “not many changes”.

Hybrid Animation. Participants were able to identify, with little effort, the stable and unstable sections of the network, the nodes that connected different parts of the network together, and the overall network evolution trend. Their description of the network evolution was less rushed. The participants mentioned that the dense sections of the network were “hard to follow and explain”. However, they were still able to explain individual connectivity within the dense network which wasn’t the case in event and hybrid tasks.

8 Scalability

We explore how scalability affects each of the animation strategies by varying the volume of data (i.e., number of events) and the time interval in which they occur. Testing user perception of a wide range of event counts and intervals with a user study would be unrealistic due to the large number of possible variables. Instead, we ran a simulation of each animation strategy for one minute. For the time-based animation strategy, the events are shown at a rate of 1 event per 8 seconds. This means that the number of events a user can perceive in a given time.

We vary the volume of data (i.e., the number of events) from 1 to 10 events at a time, and vary the time interval over which these chunks of events occur from 8 seconds down to 0.001s. The results of our simulation are shown in Figure 7. The dashed line at the 2 second mark represents the point when the rate at which events occur is greater than the rate at which they are shown in the animation. The number of events that occur is mapped to the y-axis, the time taken for each interval is mapped to the x-axis, and color is mapped to either the time delay (for event-based and hybrid animations) or number of events displayed per animation cycle (for time-based animations).

We see a staircase effect for the time-based strategy results (Fig. 7). Intervals longer than 2 seconds follow a predictable pattern of being dependent on the number of events in that interval as there is enough time for the animation cycle to complete before new events occur. With an increase in the number of events occurring per interval, the ability to perceive the events quickly declines as the events exceed 5 per interval.

The simulation results for event-based and hybrid strategies in Fig. 7 show a similar staircase effect that extends beyond the animation cycle of 2 seconds. Since there is a cap of 5 events that can occur per any animation cycle, multiple cycles are needed to handle a high volume of data. In either case, a pile-up of events occurs to the point that the animation cycles can not keep up. For instance, 10 events occurring every two second interval means that this set of events will take up the next two animation intervals, during which time, 20 more events have accumulated. The event-based strategy shows an offset at the bottom when fewer than five events occur over a standard animation cycle. That cycle will not be triggered until five events occur over a standard animation cycle. This simulation confirms our notion that the hybrid strategy eliminates the inordinate delays that we see in event-based animations with low event rates, and works in a manner similar to event-based strategy at higher event rates. It also indicates that the hybrid strategy’s timeliness is not better than event-based strategy for high event rates.

9 Discussion

We will first summarize the results from our analyses before explaining and generalizing them. Of our proposed hypotheses, we find:
Event-based staging showed significantly shorter response times compared to time-based staging, but not compared to hybrid staging for two of the three monitoring tasks. Hybrid staging showed shorter response times than time-based staging for one monitoring task (partially confirming H1).

- Participant responses to comprehension tasks showed no significant differences for tasks T4 and T5. These results reject H2a and H2b.
- Participant responses to the NASA TLX showed no significant difference in participant perception of performance, but a significantly higher level of frustration in time-based staging compared to the remaining conditions, and in hybrid staging compared to event-based staging (partially confirming H3a).
- Participants also reported significantly higher mental, physical and temporal loads and effort on time-based staging compared to the remaining two (confirming H3b). They also reported higher physical load and effort in event-based staging compared to hybrid staging.

9.1 Explaining the Results

We had posited that timeliness (R1), mental map preservation (R2), and while T2 and T3 involved graphs with nodes labeled as first names of participants observed that event-based animations sometimes had little or no animations, such as changes in network size and cluster stability. Participants also reported significantly higher mental, physical, and temporal loads and effort on time-based staging compared to the remaining conditions (confirming H3b). They also reported higher physical load and effort in event-based staging compared to hybrid staging.

9.1.1 Monitoring Tasks

The three monitoring tasks were each designed to involve more complex monitoring than the previous task, with fewer changes to the graph in T1, and more and more complex changes over longer time durations (see Table 2). In addition, T1 was an abstract task with unlabeled nodes, while T2 and T3 involved graphs with nodes labeled as first names of people. Specifically, T2 simply required participants to look for the appearance of one (named) node, while T3 required them to look for two named nodes, track them, and respond when they connect. It is very likely that the differences between staging conditions were less significant for easier and “familiar” tasks (such as T2) while they were more pronounced for more complex tasks (T3). While differences between the hybrid and event-based strategies do not emerge even for the complex monitoring task (T3), the answer perhaps lies in the comprehension task results.

9.1.2 Comprehension Tasks

The argument of complexity can be made to explain the results of the comprehension tasks as well. Of the first two comprehension tasks, T4 appears to be too complex with an almost equal distribution of right and wrong answers regardless of the condition. T5 appears to be too straightforward, with most participants answering correctly regardless of condition. T4 gives participants the label of a node to track, and requires them to first seek out the node once the video starts (the node appears after the start of the video), and keep track of it, remembering the changes in its degree. Participants performed poorly regardless of the condition likely because of their failure to identify the node in time, missing early changes to the node’s degree. T5 demands the least from the participant’s perception and memory as the cluster is labeled and does not go through complex changes (it grows and splits).

While the follow-up study with expert participants was not quantitatively evaluated, it appears to validate our reasoning: participants could only make general observations about the network in time-based animations, such as changes in network size and cluster stability. Participants observed that event-based animations sometimes had little or no changes occur over certain periods, while their impression of hybrid animations fell somewhere between the two, skewing towards event-based animation. This observation is supported by the scalability simulation discussed in Sect. 8. Given the limitation posed by the number of perceivable events [40], the hybrid strategy cannot be more “timely” than event-based strategy for high event occurrence rates. Other strategies that use Gestalt principles of completeness and common fate need to be adopted to group related events together so that they are perceived as one event. This can theoretically improve the users’ perception of multiple events, though it may come at the risk of reduced perception of anomalous activity.

9.1.3 Participant Experience

Responses on the NASA TLX scale were as predicted, except for “performance”, the mixed responses for which could be because participants were not informed whether they had the correct answer.

9.2 Generalizing the Results

Overall, event-based tasks scored well on participant preference as they reduced the load on participant perception (R2). On the other hand, Fig.[3] clearly shows that time-based strategies are best for timeliness (R1), which is achieved without compromising comprehension in the case of low data influx. The hybrid approach tends to bridge this gap between timeliness and comprehension by providing both event-based and time-based thresholds. An adaptive hybrid strategy that combines shorter time thresholds with a higher event threshold or vice versa has the potential—with judicious threshold choices—to provide the regularity of updates and the timeliness of time-based transitions for low data influx, and the ease of comprehension for high data influx. Even in the case of a monitoring task, we see from the study that comprehension is to be prioritized over timeliness.

It is worth noting that the general approach of binning—used for any staged animation—comes at the expense of information loss within the bins. This includes event order within the bin, and entire events themselves—such as nodes appearing and disappearing within the binned intervals. The limitations can be overcome by coupling additional views and metrics to track behaviors within a bin window and notify the user when such instances occur. The effectiveness of these staging alone will vary on the volume and rate of the incoming data. With higher rates of data influx, an adaptive staging strategy that adapts to the complexity of the changes. For instance, a large change can still be simple if the change is of one kind, e.g., a cluster of nodes being added to the network. Another approach would be to combine such an adaptive staging (for higher data influx rates) with time-based staging (for lower rates), to reduce the animation lag. At any rate, animation alone is not sufficient to monitor and comprehend online dynamic networks. Instead, it might work to the dashboard designer’s advantage to prioritize comprehension when it comes to animation staging, and provide supporting views for monitoring tasks.

10 LIMITATIONS AND FUTURE WORK

Through our study we learned that regardless of monitoring or comprehension tasks, animation staging strategies that prioritize comprehension do better for participant response times, accuracy, and comfort. Yet, the differences between the staging strategies are slightly blurred for tasks that are less complex or require less monitoring time. In addition, our hybrid strategy was a simple combination of the parameters used in the time-based and event-based strategies.

How event- and time-based parameters are combined for the hybrid strategy—and the user’s awareness of the strategy—could impact monitoring tasks. In our study, participants were not informed of the delays between the actual event times and when they were shown in the animations (black bars in Fig. 3). Their perception of their response time to the event was thus different from the actual response time to the event. In addition, we used constant time/event thresholds for each animation strategy for our study. We plan to explore the design space of adaptive strategies discussed in the previous section, along with indicators for animation lags in the future. In addition, we plan to explore using these staging strategies to capture network “states” that will then be visualized as static, small multiples visualizations to be used for post-event analysis. Lastly, we plan to incorporate the hybrid staging strategy into a visual analytic system for analyzing online dynamic networks to examine its applicability in real-world scenarios.

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