Spatial-Temporal Heterogeneity of Rock Samples’ Deformation and Damage: Experimental Study and Digital Image Correlation Analysis

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Research Article

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DOI: https://doi.org/10.21203/rs.3.rs-462119/v1

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Spatial-Temporal Heterogeneity of Rock Samples’ Deformation and Damage: Experimental Study and Digital Image Correlation Analysis

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Abstract: In-situ observations and laboratory experiments showed that slow deformation waves widely exist in geomedia under loading conditions. Slow deformation waves’ behavior exhibits some similarities in media ranging from the scale as large as the Earth's crust to the scale as small as the laboratory test samples. However, the mechanism underlying their generation has not been clarified yet. In this research an experimental study was performed on small-scale red sandstone samples subjected to uniaxial compression at the displacement rates of 0.1, 0.5, and 1 mm/min. Slow deformation waves under different loading rates were analyzed by speckle photography for microscopic characterization combined with the digital image correlation (DIC) technique. The Luders deformation bands were predominantly observed in the flow channels formed at the stage of macro-elastic deformation. The spatial-temporal heterogeneity of the rock sample surface was quantified, and the deformation waves' propagation velocities under different loading rates were obtained. The linear relationship between the propagation velocities of slow deformation waves and the loading rates was determined. The research findings shed some new lights on the evolutionary characteristics of the slow deformation waves.

Keywords: Rocks; deformation waves; heterogeneity; loading rate; DIC technique

1. Introduction
In-situ observations showed that slow deformation waves with propagation velocities much lower than those of transverse and longitudinal waves generated by earthquakes exist in Earth’s crust. Slow deformation waves have different names with less essential difference, for example, seismoactive waves (Mogi 1973), creeping stress waves (Savage 1971), tectonic waves (Elsasser 1969; Kasahara 1981), plastic flow waves (Wang 1993; Wang and Zhang 1994) etc. According to the concept of epicenter migration-related waves (Richter 1958), their propagation velocities in the seismic belt may reach only several dozens of kilometers per year (Levina and Ruzhich 2015; Elsasser 1969). The presence of creeping waves can be related to the instability caused by frictional sliding (Ruina 1983). As to the occurrence mechanism of these waves, it is believed that they are jointly triggered by external factors and the changes in the properties of the media in the focal area (Feng 1986).

Inside the Earth's crust, there is an interlayer composed of volatile media. Under certain conditions, the propagation of slow deformation waves may be triggered in such volatile media, and they play a crucial role in seismic development and occurrence (Geng and Xu 1990). Studies on the plastic-flow network and plastic flow waves of the continental lithosphere (Wang and Zhang 1994; Wang 1993) have shown that the driving force at the margin of the continental plate is transmitted over a long distance, primarily through the network-like flow and slow deformation waves in the lower lithosphere, including the lower crust and lithospheric mantle. This driving force also controls the intraplate deformation and seismic activities. Under the Indian plate's pushing effect, the deformation flow waves with different quasi-periodicity are present in the central and eastern Asian continent, such as ten-year and one-hundred-year period waves.

Deformation and failure of solids under the action of external factors are among the top research concerns in materials science and engineering (Shan et al.2000; Qi et al.2016). In recent years, both the spatial and temporal scales of deformation and failure of solids studied by the researchers have constantly been expanding (Qi et al.2009). (Qi et al.2017) applied the continuous phase transition theory and the Lagrangian mechanics theory to construct a theoretical model of slow deformation waves in rock surrounding deep level tunnel. The scales related to slow deformation waves may range from global to atomic scales, and the types of loading causing the deformation and failure vary from short-term (rapid) loading to long-term one (at creep rates) (Li et al.2008; Li et al.2019). The theoretical study (Li and Shao 2016) applied the multi-microcrack model to
study the macroscopic brittle creep failure caused by microcrack growth under step loading and unloading in rocks.

During large-scale field observations, significant variations of the geophysical field's spatial-temporal characteristics were measured to determine slow waves' features. It was found that the directional migration of the epicenter was a prevalent phenomenon, which could be observed, for example, in the Hindu Kush region (Malamud and Nikolaevsky 1985, 1989), in Baikal Lake region of Siberia (Sherman and Gorbunova 2008; Levina and Ruzhich 2015; Psakhie 2001), and in China (Wang 1987; Wang et al. 1990; Wang and Zhang 2004). Fig. 1 shows the propagation path of slow deformation waves originated from the Himalayan Arc (Wang 1987).

As to the deformation waves at the laboratory level, compression and tensile tests have been performed for the sylvite, marble, and alkali halide samples. The slow deformation waves traveling in the samples were studied (Barannikova et al. 2010; Zuev et al. 2012). It was found that the slow deformation waves traveling in the rock samples and the alkali halide samples were similar to those observed previously in the metallic materials (Zuev and Danilov 1997). All of these findings are of high significance to the study of slow deformation waves in geomaterials.

Most of the existing experimental studies on the slow deformation waves have been conducted on such homogeneous materials as metals or metal halides, but less commonly on rocks. The propagation and evolution characteristics of the deformation waves in rocks have not yet been adequately studied. The microscopic and mesoscopic mechanism of the slow deformation wave has not been clearly explained. The relationship between the propagation speed of the slow deformation wave in the rock and the loading rate has not been specifically studied. Since slow deformation waves mainly propagate in the Earth's crust, typically through rocks as the media, it is important to study their propagation and evolution in rocks. In the present study, indoor uniaxial loading tests were performed for a group of red sandstone samples under the loading rates of 0.1, 0.5, and 1 mm/min, respectively. In process of deformation and failure of the rock samples, speckle photography technique combined with the digital image correlation (DIC) technique were used to quantify the slow deformation waves. The evolution of the strain component $\varepsilon_{xx}$ under the three loading rates was studied, and the propagation rates of the deformation waves under different loading rates were calculated. The relationships
between the wave propagation velocity and loading rate were further analyzed. The analysis of obtained nephograms indicated that the Luders deformation occurred predominantly in the flow channels formed at the stage of macro-elastic deformation. It was related to the extreme values of the elastic standing waves.

2. Experiments

2.1 Test equipment and rock samples

The rock samples under study correspond to the third category of the red sandstone. The latter exists in two main structure forms, including granular-clastic and mud cement forms, and has high hygroscopicity, porosity ranging approximately from 0.1 to 0.3, low bonding performance, poor overall performance, and is less prone to disintegration than ordinary sandstone. Nine red sandstone samples with dimensions of 50mm×50mm×100mm were prepared using the method recommended by the International Society for Rock Mechanics (ISRM) (Fairhurst and Hudson 1999). Every two opposite sides were parallel to each other, and all of them were smooth. All samples were prepared from the same batch of blocks harvested on-site. Those with defects and joints were eliminated.

The rock samples were subdivided into three groups, each containing three samples, and were subjected to displacement-controlled compressive loading at three loading rates, using a DRTS-500 test bench composed of the loading system (with the maximum axial load of 500KN) and the data collection system. The displacement control mode was adopted since the test goal was to investigate slow deformation waves under different loading rates. The rock sample geometry and the experimental equipment are shown in Fig. 2.

Fig.2

Given that speckle photography was adopted to capture the rock samples' images, the samples were first sprayed with a layer of ordinary white paint and left to dry. Then, another layer of black particle paint was sprayed to form random speckles (Munoz et al. 2016; Heinz and Wiggins 2010; Yang et al. 2015).

2.2. Experimental scheme

Before the main displacement-controlled tests, a group of uniaxial compression tests was first performed to obtain the basic mechanical parameters of rock samples. The average compressive strength of the rock samples
was 80 MPa. The loading was imposed under the displacement-controlled mode with three different rates: 0.1, 0.5, and 1 mm/min, respectively. In each group, speckle photography was used for microscopic characterization from the start to the end of the loading process. Later, the collected images were subjected to the digital image correlation (DIC) analysis. The evolution of the displacement vector $\mathbf{r}(x, y)$ field at the marked points on the sample surface was tracked and recorded to provide data for the further analysis.

The stress-strain curves of the rock samples obtained from the uniaxial compression tests are shown in Fig. 3, where $\varepsilon_1$ is the axial strain; $\varepsilon_3$ is the transverse strain; and $\varepsilon_v$ is the volumetric strain. The pressure in the figure below is defined as positive. A typical stress-strain curve of an intact rock sample can be roughly subdivided into the following four stages. The first stage is the compaction stage, where the curve bends slightly upwards, and the initial microcracks are closed due to the compression. The curve is a straight line at the second stage, so this is the linear elastic stage. At the third stage, the curve bends slightly downwards, and unstable microcracks are generated in the direction parallel to the loading direction. The third stage is called a non-elastic (plastic) stage, while the fourth one is referred to as the failure stage. At the plastic and failure stages, cracks appeared on the sample surface, so the DIC technology would fail to achieve the desired effect. Therefore, DIC is only applicable to the data at the first two (compaction and elastic) stages. In metals and alloys, features of strain localization that resemble those of the deformation waves have been observed at the linear elastic stage in the samples under compression or tension (Danilov et al. 2005, 2009). In the present study, the deformation waves' propagation velocities at the linear elastic stage (segment AB in Fig. 3) were of the primary concern during the loading process. At this stage, the wave propagation velocity was closer to the slow waves velocities observed in Earth’s crust and exhibited similar evolution patterns.

### 2.3 Technical principle of DIC

Digital image correlation (DIC) technique is a non-contact optical technique known for its practicability and effectiveness (Peters and Ranson 1982). This technology can be used to measure the deformation of an object's surface. Currently, DIC has been widely applied to experimental studies on the deformation of rocks and rock-like materials (Munoz et al. 2016; Stirling et al. 2013; Lin et al. 2019; Miao et al. 2018; Lin et al. 2019; Zhao et al. 2018; Zhou et al. 2018). The core algorithm used in the DIC tracks the relative displacement of the speckles
by comparing the current image against the reference one, as shown in Fig. 4. The reference image is subdivided into smaller subsets, whose changes are tracked on the deformation images. The $x$ and $y$ coordinates of the point $P_{\text{cur}}(x_{\text{cur}}, y_{\text{cur}})$ in the current subset are related to the coordinates of the point $P_{\text{ref}}(x_{\text{ref}}, y_{\text{ref}})$ in the reference subset as follows:

$$x_{\text{cur}} = x_{\text{ref}} + u_{\text{rc}} + \frac{\partial u}{\partial x_{\text{rc}}}(x_{\text{ref}} - x_{\text{refc}}) + \frac{\partial u}{\partial y_{\text{rc}}}(y_{\text{ref}} - y_{\text{refc}})$$

(1)

$$y_{\text{cur}} = y_{\text{ref}} - v_{\text{rc}} + \frac{\partial v}{\partial x_{\text{rc}}}(x_{\text{ref}} - x_{\text{refc}}) + \frac{\partial v}{\partial y_{\text{rc}}}(y_{\text{ref}} - y_{\text{refc}})$$

(2)

where $x_{\text{ref}}$ and $y_{\text{ref}}$ are the $x$ and $y$ coordinates of the point $P_{\text{ref}}$ in the reference subset, respectively; $x_{\text{refc}}$ and $y_{\text{refc}}$ are the $x$ and $y$ coordinates of the central point $Q_{\text{ref}}$ in the reference subset, respectively; $u_{\text{rc}}$ and $v_{\text{rc}}$ are the horizontal and vertical displacements of the subset, respectively; $\frac{\partial u}{\partial x_{\text{rc}}}$, $\frac{\partial u}{\partial y_{\text{rc}}}$, $\frac{\partial v}{\partial x_{\text{rc}}}$, and $\frac{\partial v}{\partial y_{\text{rc}}}$ are the gradients of the subset's displacement components, respectively.

2.4 Calculation of different strain components

Different strain components are calculated as follows:

$$\nabla r = \beta_{ij} = \begin{bmatrix} \epsilon_{xx} & \epsilon_{xy} \\ \epsilon_{yx} & \epsilon_{yy} \end{bmatrix} + \omega_z$$

(3)

where $\epsilon_{xx} = \frac{\partial u}{\partial x}$ is the strain vector component along the compression direction $x$, $\epsilon_{yy} = \frac{\partial v}{\partial y}$ is the transverse strain component, $\epsilon_{xy} = \epsilon_{yx} = \frac{1}{2} \left( \frac{\partial u}{\partial y} + \frac{\partial v}{\partial x} \right)$ is the shear strain component, $\omega_z = \frac{1}{2} \left( \frac{\partial u}{\partial y} - \frac{\partial v}{\partial x} \right)$ is the rotational component, while $u$ and $v$ are the components of the displacement vector $r$ along the $x$- and $y$-axes, respectively.

3. Experimental Results

3.1 The slow-wave propagation pattern at the compaction stage

The rock samples’ DIC data were studied at the first (compaction) stage at three loading rates (0.1, 0.5, and 1mm/min). The variation of the strain component $\epsilon_{xx}$ on the sample surface at the initial stage of loading were analyzed. Here, the 3D diagrams and vertical views of the rock samples under the loading rate of 0.1mm/min at the two time moments are presented and described in detail. Only the vertical views of the experimental results under the two loading rates (0.5 and 1mm/min) are presented due to limited space.
Figure 5 shows the strains at two time moments at the compaction stage under the loading rate of 0.1 mm/min. The left side is the end of sample, to which the load was applied. The first column shows the 3D diagrams of strain, from which the strain of the sample could be intuitively observed at a specific time moment for the sample under loading. The second column shows the vertical view of the diagram corresponding to the first column, from which the maximum strain and strain fluctuations along the length of the sample can be obtained. It can be seen from the 3D diagram in Fig. 5a that the irregular strain fluctuations occurred throughout the entire stage. The fluctuations were more significant on the left side and gradually attenuated towards the right one. From the vertical view, it could also be observed that after applying load, strains with more significant fluctuations first appeared on the left side at the initial stage. By contrast, the fluctuations were milder on the right side, and the fluctuations were not synchronized on the left and right sides. At the distance 60-70mm from the left side end, there was an isolated peak of compressive strain. Such fluctuation pattern, which occurred in the form of a single moving peak, resembled a solitary wave or surge wave (Qian 1985), i.e., a gravity wave, which is generally caused by the inertial force and gravity.

According to Fig. 5a, the strain values over the entire sample surface fluctuated consistently in the 3D diagram. Except for the leftmost side, there was no significant difference in the strain values within this region. As shown by the vertical view, the strain values fluctuated in a wave-like pattern. However, after the peak at the distance 65 mm from the left side end, the fluctuations were less significant than those on the left side. Although the strain values increased, the fluctuations were obscure and less regular. The strain values were slightly higher at the two ends. In Fig. 5b, several large strain peaks occurred and showed a dispersed distribution. Their spatial distribution was non-uniform and disordered. Compared with Figure 5a, there are several complete wave fluctuations between the 65mm-100mm, and the fluctuations are clear and obvious. According to the vertical views in Fig. 5a and 5b, as loading continued, the fluctuations became more pronounced, and the degree of waviness increased. The peak values gradually increased and occurred more frequently. Moreover, the waviness became increasingly apparent.

It is noteworthy that as the loading rate increased, the fluctuations on the left half side became more intensive. The peaks were also greater and denser. At the loading rate of 1 mm/min, the sample surface was subjected to a greater pressure than at other loading rates. As a result, the maximum strain occurred instantaneously in the
left corner, its value being approximately five times the strain values at other places on the same surface (Fig. 6).

Fig. 6

Taken together, whatever the loading rate is, the strain component was greater at the end to which the load was applied but smaller at the other end. As the loading continued, the strain components at both ends became more consistent. During this process, the slow deformation wave propagated through the media, accompanied by energy accumulation and conversion. The slow deformation waves were generated by adjusting the imbalance between the driving force and the viscous force inherent inside the solids. This process involved the conversion between the elastic strain and kinetic energies.

3.2 Wave characteristics at the same strain under different loading rates

The strain data were analyzed at the strain level of 0.006 under the three loading rates. Figures 7a, 7b, and 7c present the 3D strain diagrams under the loading rates of 0.1, 0.5, and 1 mm/min, respectively. The vertical views are compared to the strain diagrams along the sample surface's central line, as shown in Fig. 7.

Fig. 7

Comparison of the 3D strain diagrams under the three loading rates indicated spatial-temporal heterogeneity and disorderedness. The fluctuations were more significant on the 3D strain diagram under the loading rate of 0.1 mm/min (Fig. 7a) than under the other two loading rates. A comparison of the vertical views showed that the deformation waves' peaks were denser on the strain diagrams under the loading rates of 0.1 and 1 mm/min (Fig. 7a and 7c). By contrast, there were much fewer peaks in Fig. 7b, indicating more regular and consistent strain fluctuations on the sample surface. The strain diagrams along the central line of the sample surface were analyzed under the three loading rates. The fluctuation is obvious from the left boundary to 65mm in Fig. 7a. However, the fluctuations barely existed in the second half, indicating that the deformation wave had not yet propagated to the second half. By contrast, the fluctuation in Figure 7c is not so regular, and there is no obvious fluctuation period. As compared with the cases of other two loading rates, the waves undulates gently. Thus, the deformation waves' fluctuations were much more regular in the red sandstone samples under the loading rate of 0.5 mm/min. The propagation rate was the lowest at the loading rate of 0.1 mm/min. And at 1 mm/min, the deformation wave propagates in the form of broken lines.
3.3 Strain nephograms of the deformation waves

Fig. 8
Fig. 9

Four time moments at the compaction and elastic stages were chosen during the loading process (see Fig. 8). The strain nephograms of the three strain components $\varepsilon_{xx}$, $\varepsilon_{yy}$, and $\varepsilon_{xy}$ are presented at these four time moments, as shown in Fig. 9. For data processing, negative strain values under compression were represented by blue and light blue in the nephograms, while positive strain values under tension were represented by red and yellow. As indicated by the strain component $\varepsilon_{xx}$, the micro-grains on the sample surface prior to loading were in a disordered and dispersed state. During the compression process, there was a region of tensile deformation between the regions of compressive deformation. As the loading continued, these micro-grains near flow channels moved closer to the flow channels (at an angle of about 60° relative to the $x$-axis, i.e., the sample axial direction. Points 1 and 2, represented by dotted lines in Fig. 9) and gradually became connected along the flow channels. These flow channels cross symmetrically with each other and are distributed in a grid pattern.

Throughout the loading process, the values of the strain components $\varepsilon_{yy}$ and $\varepsilon_{xy}$ were very small. Among them, the distribution of $\varepsilon_{yy}$ cloud image shows obvious vertical distribution characteristics, and gradually shifts to the middle with the loading time. The areas on both sides of the $\varepsilon_{xy}$ strain cloud map show periodic strong tensile deformation zones from the beginning. For example, in the nephograms (Fig. 9), corresponding to points 2 and 3 in Fig. 8, the strong tensile deformation, as indicated by the strain component $\varepsilon_{xy}$, periodically appeared at 20-60mm, with a magnitude of about 0.1% (as indicated by the arrowhead at the point 3 in Fig. 9). These regions of strong tensile deformation corresponded to the flow channels observed in the nephogram of $\varepsilon_{xx}$. This phenomenon was observed throughout the compaction and elastic stages of loading.

As observed in the nephogram of $\varepsilon_{xx}$, the nucleation of Luders bands (LB), i.e., shear bands formed in regions of stress concentration, occurred during the loading process (point 2 in Fig. 9). At first, the nuclei had small oval cross-sections and appeared in pairs. One of them was a region of compressive strain with the maximum strain value being -0.5%; the other was a region of tensile strain with the maximum strain value being 0.2%. The grain deformation and LB nucleations were more conspicuous in the nephogram of $\varepsilon_{xy}$ and observed roughly at the same positions as those in the nephogram of $\varepsilon_{xx}$. The maximum strain value was 0.15%. The observed nucleation pattern can be explained as follows. The displacements originated from the
sample surface, whose deformation exceeded the bulk one, i.e., the average deformation of the sample. During
the sample's loading-induced deformation, the displacement was rapidly released, thereby resulting in the LB
nucleation.

After grain deformation and LB nucleation, the Luders bands were gradually formed. In the beginning, the
Luders bands were obscure. As the loading continued, the Luders bands became clearer and began to show
more conspicuous banding features. This trend started from both sides of the sample simultaneously, with slow
interconnection and penetration in the transverse direction. This phenomenon indicated that the Luders bands
were already formed (points 3 and 4 in the nephogram of $\varepsilon_{xx}$ in Fig. 9) before the plastic deformation stage.
The Luders bands were mainly concentrated on the half part of the sample near the end where the load was
applied; however, the strain was smaller on the other half part. This situation was not observed on the
nephograms of $\varepsilon_{yy}$ and $\varepsilon_{xy}$.

On the nephogram of the $\varepsilon_{xy}$ component near the left side of the sample, the strain concentration were
periodically distributed at an interval of about 10 mm (as indicated by the arrowheads at points 1 and 2 in Fig.
9). The deformation (probably, a plastic one) at these central points was about 0.5%. Between these points,
there were points with the opposite sign of $\varepsilon_{xy}$ component, which were treated as nodes of elastic standing
waves in the samples under loading (points of maximum and minimum values). The points marking the flow
channels and the nodes of elastic standing waves that appeared at the compaction and linear elastic stages
remained active throughout the entire loading process. This indicated the conversion between the plastic and
elastic deformation standing waves.

As to the component $\varepsilon_{xx}$, the flow channels were parallel to the Luders bands. However, the Luders bands
and the initial stress concentrators (i.e., nucleation sites) were located outside the flow channels. From this, we
inferred that they were of different origins.

Fig. 10

Three points were chosen along the sample's axis, namely, at 30, 50, and 70 mm (positions of these points
are shown in the nephogram of $\varepsilon_{xx}$ at point 3 in Fig. 9). The temporal variations of the axial strain components
at these three points during the loading process were tracked and represented, as shown in Fig. 10. The curves
in Fig. 10 depict fluctuations of the vertical strain component during the loading process. Generally speaking,
the deformation is greater near the end when the load was applied and smaller farther away from this end. At
30 mm, 0.3%<\(\varepsilon_{xx}\)<0.35%; at 50mm, 0.35%<\(\varepsilon_{xx}\)<0.4%; at 70mm, 0.4%<\(\varepsilon_{xx}\)<0.48%. These three points were
close to the three flow channels generated during the loading process (Fig. 9).

Thus, the maximum deformation amplitudes of the three flow channels can be ranked as follows:
\[\varepsilon_{xx}^{\text{max}}(\text{FC1}) > \varepsilon_{xx}^{\text{max}}(\text{FC2}) > \varepsilon_{xx}^{\text{max}}(\text{FC3}).\] They are determined by their duration. The longer the time it appears,
the greater its deformation. As the width of the Luders bands increased, these three flow channels successively
entered active deformation regime. Therefore, it was presumed that the Luders bands' formation was related to
the flow channels' maximum strain value. As the deformation was intensified, the Luders bands interacted with
the flow channels nearby to generate the maximum strain values.

3.4 Propagation velocity analysis of the deformation waves at the elastic stage

Deformation waves are generated during the loading process of the red sandstone samples. Some researchers
have studied the propagation of deformation waves and estimated their propagation velocity range. However,
the relationships between the propagation velocities of the deformation waves and the loading rates have not
been fully clarified. In our study, such relationships were determined based on the experimental data.

Deformation waves has one unique feature: it propagates along the sample's axis. The loading diagram is
shown in Fig. 11. Since the samples were loaded at a steady loading rate, an approximate dependence \(\varepsilon\sim t\) was
assumed. The deformation waves' strain peaks (i.e., peaks and troughs of the deformation waves) were plotted
on the X-axis. The slope of the straight line representing the relationship of \(X\) vs. \(t\) was calculated. On this basis,
the motion velocities of points with the maximum and minimum values of strain, that is, the propagation
velocities of the deformation waves, were estimated.

Taking the case with a loading rate of 0.5 mm/min as an example. After the microscopic characterization of
the specimen, the deformation diagram of the strain component \(\varepsilon_{xx}\) on the centerline at 8 time moments was
selected in the elastic stage (Fig. 12). According to the treatment method of local strain maximization, the points
of local strain maximum are chosen for comparative analysis. The results are shown in Fig. 13.
After data processing, the deformation wave's propagation velocities were estimated as $5.4 \times 10^{-5}$, $6.0 \times 10^{-5}$, and $6.3 \times 10^{-5}$ m/s in the three groups of experiments under the loading rate of 0.5 mm/min. After averaging, the strain peak's propagation velocity (of deformation waves) was $5.9 \times 10^{-5}$ m/s in the samples. It exceeded the axial boundary advance propagation velocity of $0.8 \times 10^{-6}$ m/s (equivalent to the loading rate of 0.5 mm/min) by one order of magnitude. Therefore, the propagation velocities of the deformation waves was significantly higher than that of the matter particles.

The propagation velocity of the slow deformation waves was calculated under the loading rate of 0.5 mm/min. Under this loading rate, stable regions of localized deformation were formed due to the slow deformation waves. These regions did not move over time. It can be observed from the dashed box in Fig. 12 that at 60-100 mm on the sample surface, the peaks and troughs' positions were relatively fixed, and the peak and the basic shape of the wave only change slightly. However, the waveform and the peaks' positions changed significantly for the regions formed at an earlier stage, indicating the normal propagation and fluctuations. This situation persisted until the last diagram. The above region was stable and no longer experienced dramatic plastic deformation over time. The propagation of slow deformation wave occurs at the initial stage of loading, that is, the elastic stage and the compaction stage. At the initial stage, the damage of the sample develops uniformly, and the slow deformation wave propagation is produced. As the loading process goes on, the plastic localization occurs gradually, and the propagation of slow deformation wave no longer appears. At this stage, the plastic deformation is concentrated to the adjacent weak points, thus showing the plastic localization, and then these weak points are gradually connected, resulting in the fracture of a plane.

Using the same method, the propagation velocities of the deformation waves in the three groups of samples under the loading rate of 0.1 mm/min were estimated as $3.0 \times 10^{-5}$, $3.3 \times 10^{-5}$, and $3.5 \times 10^{-5}$ m/s, respectively. The average wave propagation velocity was $3.27 \times 10^{-5}$ m/s. Under the loading rate of 1 mm/min, the propagation velocities of the deformation waves in the three tested samples were $10.1 \times 10^{-5}$, $10.5 \times 10^{-5}$, and $10.7 \times 10^{-5}$ m/s, respectively, and the average velocity was $10.4 \times 10^{-5}$ m/s. The wave propagation velocities under the three loading rates were roughly equivalent to those of the plastic flow waves controlling earthquake migration in the lower lithosphere (Wang 1994).
The deformation waves’ propagation velocities obtained at the loading rates of 0.1, 0.5, and 1 mm/min by testing nine samples are plotted in Fig. 14. As the loading rate increases, the propagation velocities of the deformation waves increases linearly. Thus, a positive linear correlation between these parameters with a high correlation coefficient $R^2=0.9964$ was revealed. The above dependence was best-fitted by a linear regression formula presented in Fig. 14.

Fig. 14

4. Discussion

Various experimental tools tracked the spatial-temporal occurrences of the deformation waves in the deformed red sandstone samples during their loading. The generation of deformation waves in the rock samples was found to be related to the regions of elastic stress concentration of varying scales (Farber et al. 2019). Under the three loading rates, the deformation waves’ propagation rates were $3.0 \times 10^{-5}$, $5.9 \times 10^{-5}$, and $10.4 \times 10^{-5}$ m/s, respectively. They exceed by one order of magnitude the axial loading rates, i.e., the boundary advance speeds, of $0.16 \times 10^{-6}$, $0.8 \times 10^{-6}$, and $1.6 \times 10^{-6}$ m/s, respectively, for the loading rates of 0.1, 0.5, and 1 mm/min. Thus, the propagation rate of deformation waves is significantly higher than that of the mass particles. The local thickening and uplift caused by boundary advancement continue to propagate with the help of elastic force and inertial force. Thus, the matter particles’ initial high displacement rate under the elastic force's action tended to decrease due to viscous resistance. As the flow rate decreased, the subsequent substance deformation was accumulated, leading to local bulging and increased elastic potential. This would further accelerate the matter particles’ displacement velocity. Such alternation of high and low velocities is manifested as wave propagation.

It can be considered that this is a kind of deformation wave that contains the migration of matter particles which is essentially the particle momentum waves proposed by Fitzgerald (1966).

The deformation wave propagation is a process of mutual conversion between the elastic and kinetic energies under the boundary-driven condition and a process of adjustment for the imbalance between the driving force and viscous force inherent in solids. The situation where the driving boundary induces the deformation wave propagation is known as "boundary-driven wave generation" or "external-driven wave generation". Viscous deformation arises when the elastic stress is relaxed in regions of stress concentration (Farber 2002). The elastic strain concentration is restricted by viscous deformation (relaxation). Moreover, since the viscous
deformation is usually induced near the regions of stress concentration, the distribution of centers of viscous
deformation (flow channels) in the samples coincided with those of the regions of elastic strain concentration.

5. Conclusions

In the present study, rock samples were subjected to microscopic characterization by speckle photography
during the uniaxial compression test. The image processing via the DIC technology revealed the spatial-
temporal evolution of the deformed samples' deformation waves. The characteristics of deformation waves in
the samples under loading were obtained as follows:

(1) The deformation waves slowly propagated from one end of the sample, to which the load was applied. The strain magnitude was much higher at one end to which the load was applied than that at the other one at the beginning of loading. However, the strain values became comparable over time over the sample, thus demonstrating deformation wave propagation in the laboratory tests of small-scale rock samples.

(2) In the samples under loading, the deformation waves are influenced by the elastic standing waves, which could be inferred from the positions of the minimums and maximums of the elastic standing waves (regions of stress concentration) and the flow channels' distributions. These flow channels were formed at the compaction and elastic stages and were involved in the subsequent stages. As the stress increased, the LB nuclei interacted with the flow channels nearby to generate the minimum and maximum strain values ($\varepsilon_{xx}$).

(3) As the loading rate increased, the propagation velocity of the deformation waves increased linearly. Thus, a positive linear correlation between these parameters with a high correlation coefficient $R^2=0.9964$ was revealed.

(4) The experiments and comparative analyses conducted in this paper were semi-quantitative ones, and further investigations are needed in this respect. The research findings shed some new lights on the evolutionary characteristics of slow deformation waves and earthquake migration. They also provide experimental data for more in-depth analysis of the generation and propagation mechanism of slow deformation waves in the continental plates.

Acknowledgments
This work was supported by the National key basic research development plan (approval No.: 802015CB575), National Natural Science Foundation of China (approval No.: 51774018), and Yangtze River scholars innovation team program (PCSIRT, IRT_17R06).

**Data Availability Statement**

Some or all data, models, or code that support the findings of this study are available from the corresponding author upon reasonable request.

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**Figure 1**

Propagation of slow waves originated from the Himalayan Arc in the East Asian continent (Wang 1987, Wang et al. 1990) Note: The designations employed and the presentation of the material on this map do not imply the expression of any opinion whatsoever on the part of Research Square concerning the legal status of any country, territory, city or area or of its authorities, or concerning the delimitation of its frontiers or boundaries. This map has been provided by the authors.
Figure 2

Red sandstone samples and relevant experimental equipment (a) The rock samples, (b) Loading and speckle photography system, (c) Local image of loading
Figure 3

Stress-strain curves of the rock samples and the corresponding stress thresholds (Brace et al. 1966, Martin and Chandler 1994, Fu et al. 2020)
Figure 4

Schematic of the DIC technology (Blaber et al. 2015)

Three-dimensional diagram

Elevation
Figure 5

Strain characterization of the rock samples at different time points under the loading rate of 0.1 mm/min

Deformation wave elevation of strain component $\varepsilon_{xx}$

- $v=0.5$ mm/min
- $v=1$ mm/min

Figure 6

Vertical view of the strain component $e_{xx}$ at different time points at loading rates of 0.5 and 1 mm/min
Figure 7

Strain diagrams at the same strain under different loading rates
Figure 8

Stress-strain and stress-time curves at a loading rate of 0.1 mm/min
Figure 9

Strain nephograms corresponding to points 1 to 4 of the stress-strain curve in Fig. 8
Figure 10

Variations of the strain component $\varepsilon_{xx}$ over time at different sites
Figure 11

The loading scheme of rock samples
Figure 12

Deformation waves along the central line of the samples from 640s to 920s
Figure 13

Variation trend of the maximum value of localized strain along the central line
Figure 14

Dependence of the propagation rate of the deformation waves on loading rate