Neural Networks-Based Adaptive Exponential Quasi-Passification and Output Tracking Control for Uncertain Switched Nonlinear Systems

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The abstract and index terms sections are provided as follows:

ABSTRACT In this paper, we mainly study the adaptive exponential quasi-passivity and adaptive tracking control of lower triangular uncertain switched nonlinear systems, even though the adaptive output tracking control problem of individual subsystem is unsolvable. First, the exponential quasipassivity concept is proposed to describe the energy changing of the overall switched nonlinear systems without the exponential quasi-passivity property of all the subsystems. Then, for switched nonlinear systems, the semiglobally uniformly ultimate boundedness is achieved by using exponential quasipassivity. Second, this result is applied to solve adaptive tracking control problem uncertain switched nonlinear systems in lower-triangular form. A new adaptive tracking control technique is developed by combining quasi-passification methods with adaptive backstepping techniques. The unknown nonlinear functions are approximated by the radial basis function neural networks. In contrast to the existing results, the multiple storage functions method reduces the conservativeness caused by a common Lyapunov function for all subsystems. Finally, the effectiveness of the proposed method is verified by an example.

INDEX TERMS Switched nonlinear systems, neural networks, output tracking control, exponential quasi-passification.

I. INTRODUCTION

The notion of passivity originated in electrical network theory was first proposed by Willems [1]. In general, passive system dissipates no more energy than the external supply. Passivity theory was widely applied in analysis and synthesis of nonlinear systems [2], [3]. This motivates the researchers [4] to establish necessary and sufficient conditions for feedback passification of nonlinear systems. In practical systems, In practical systems, structural uncertainty and other uncertainties are ubiquitous. These effects of uncertainties on plants can be eliminated with the aid of robust control and adaptive control [5], [6]. To deal with with structural uncertainties, [5] adopted robust control method to solve passification and stabilization problems. In [6], adaptive passification method was developed for nonlinear systems with parameter uncertainties. When the controlled system is considered unknown, neural networks passivity was investigated in [7], [8]. Nevertheless, the aforementioned feedback passification method is its limitation to systems with relative degree one and being minimum-phase. To overcome these restrictive conditions, [5], [9] combined backstepping technique with passification method to solve the stabilization problem of uncertain nonlinear systems. Because of the existence of the large uncertainties, it was often hard to realize exact feedback passification. In [10], [11], only passivity except for a compact region was achieved. Similar practical passivity property was investigated in [12]–[14]. [12] proposed a concept of quasi-passivity. Compared with passive systems, quasi-passive systems can produce energy itself. In [13], [14], semi-passivity was studied and applied to solve synchronization in networks of neuronal oscillators. This practical passivity was also used to solve nonlinear control problem of uncertain nonlinear systems in lower-triangular form [11], [15]. In [11],
exponential quasipassivity and backstepping technique were adopted to analyze stability of power system. In [15], based on the set passivity theory, adaptive fuzzy tracking problem was solved by backstepping technique for a class of unknown nonlinear systems with saturation input nonlinearity.

On the other hand, switched systems have received extensive research attention in recent years [16]–[23]. Many real-world systems can be modeled as switched systems [16]–[19]. Several methods were often used to investigate switched nonlinear systems [18]–[23]. Passivity is an important system property of switched systems as nonswitched systems. So far, many scholars have studied the passivity of switched systems [24]–[31]. [24] defined passivity of switched systems using a common storage function method. But it is often hard to obtain a common storage function even for each subsystem is one [29]. Finally, a more general switching law which allows the storage function increase at each switching point is designed constructively to achieve output tracking control, while the dwell time and the common Lyapunov method adopted in [20]–[22] are infeasible for the problem under study.

II. PRELIMINARIES AND PROBLEM FORMULATION
A. PRELIMINARIES
Consider a switched nonlinear system described by

\[
\begin{align*}
\dot{x} &= f_\sigma(x, u_\sigma), \\
y &= h_\sigma(x),
\end{align*}
\]

where \(x \in \mathbb{R}^n\) is the state, \(\sigma : [0, \infty) \to I = \{1, 2, \ldots, M\}\), called a switching signal, is a piecewise constant function. \(u_i \in \mathbb{R}^m\) and \(y \in \mathbb{R}^m\) are the input and output vectors of the \(i\)-th subsystem, respectively. \(f_i(\cdot)\) and \(h_i(\cdot)\) are assumed to be smooth with \(f_i(0, 0) = 0\) and \(h_i(0) = 0\). The switching signal can be characterized by

\[
\sum = \{x_0; (i_0, t_0), (i_1, t_1), \ldots, (i_k, t_k), \ldots; i_k \in I, k \in \mathbb{Z}_+\},
\]

in which \(x_0\) denotes the initial state at the initial time \(t_0\) and \(\mathbb{Z}_+\) stands for the set of non-negative integers. When \(\sigma(t) = i_k\), the \(i_k\)-th subsystem is active during \([t_k, t_{k+1})\). In addition, we assume that the state of the system (1) does not jump at the switching instants.

The definitions of class \(K_\infty\) functions, class \(GK\) function are introduced as follows.

**Definition 1** [35]: A function \(\gamma : \mathbb{R}^+ \to \mathbb{R}^+\) is called a class \(K_\infty\) function if it is continuous, positive definite, strictly increasing and \(\gamma(r) \to \infty\) as \(r \to \infty\).

**Definition 2** [19]: A function \(\alpha : \mathbb{R}_+ \to \mathbb{R}_+\) is called a class \(GK\) function if it is increasing and right continuous at the origin with \(\alpha(0) = 0\).

Next, we will give an exponential quasi-passivity definition of system (1).

**Definition 3**: System (1) is said to be exponentially quasi-passive, if, for a given switching signal \(\sigma\), there is a nonnegative function \(V(\sigma(t), x) : I \times \mathbb{R}^n \to \mathbb{R}^+\), called storage function, constants \(\lambda > 0, c_i \geq 0\), class \(GK\) function \(\alpha\) such
that
\[ e^{\lambda t}V(\sigma(t), x(t)) - e^{\lambda t_0}V(\sigma(t_0), x(t_0)) \leq \int_{t_0}^{t} e^{\lambda \tau} u_{\sigma}(\tau) \cdot y(\tau) + c_{\sigma}(\tau) d\tau + e^{\lambda t_0} \alpha(||x(t_0)||) \] (3)
holds for all the initial state \( x(t_0) \).

**Remark 1:** Obviously, system (1) is quasi-passive by letting \( \lambda = 0 \). \( c_i \) is seen as internal supply rates, which means system can produce energy by itself. If \( c_i = 0 \), Definition 2 degenerates into passivity of switched system in [27]. By (3), the energy of switched system may increase at any switching time and is bounded by \( e^{\lambda t_0} \alpha(||x(t_0)||) \).

We will investigate ultimately boundedness of system (1) using exponential quasi-passivity.

**Definition 4:** System (1) is semiglobally uniformly ultimately bounded, find, if possible, feedback controllers \( u_i, i \in I \) and a switching signal \( \sigma(t) \) such that for given any initial compact set \( \Omega \), the closed-loop system possesses the following properties:

(a) (Uniform boundedness) there exists compact set \( \Omega_x \) such that for all \( t_0 \geq 0 \), \( x(0) \in \Omega \) implies \( x(t) \in \Omega_x, \forall t \geq t_0 \).

(b) (convergence) for all initial condition \( x(0) \in \Omega \), there exists \( T \) such that states \( x(t) \) eventually converge to the compact set \( \Omega_x \), i.e., \( x(t) \in \Omega_x, \forall t \geq T \).

We will investigate ultimately boundedness of system (1) using exponential quasi-passivity.

**Lemma 1:** Suppose that system (1) is exponentially quasi-passive with a storage function \( V(\sigma(t), x) = V_\sigma(t)(x) \). If there exist class \( K \) functions \( \phi_1, \phi_2 \) satisfying \( \phi_1(||x||) \leq V_1(x) \leq \phi_2(||x||) \). Then, the closed-loop system possesses continuous functions satisfying \( \psi_i(0) = 0 \) and \( y^T \psi_i(0) \geq 0 \).

**Proof:** Since system (1) is exponentially quasi-passive, for \( t \in [t_k, t_{k+1}] \), substituting \( u_i = -\psi_i(y) \) into (3) gives
\[
\begin{align*}
\dot{e}^{\lambda t}V(\sigma(t), x(t)) - e^{\lambda t_0}V(\sigma(t_0), x(t_0)) &= e^{\lambda t}V_{\xi}(x(t)) - e^{\lambda t_0}V_0(x(t_0)) \\
&\leq \int_{t_0}^{t} e^{\lambda \tau} u_{\sigma}(\tau) \cdot y(\tau) + e^{\lambda t_0} \alpha(||x(t_0)||) \tag{4}
\end{align*}
\]
It follows from \( \phi_1(||x||) \leq V_1(x) \leq \phi_2(||x||) \) that
\[
\begin{align*}
\phi_1(||x(t)||) &\leq V_1(x) \\
&\leq e^{-\lambda(t-t_0)}V_0(x(t_0)) + e^{-\lambda(t-t_0)} \alpha(||x(t_0)||) \\
&\quad + \frac{c}{\lambda} \left( 1 - e^{-\lambda(t-t_0)} \right) \\
&\leq e^{-\lambda(t-t_0)} \left( V_0(x(t_0)) - \frac{c}{\lambda} + \alpha(||x(t_0)||) \right) + \frac{c}{\lambda} \\
&\leq \alpha(||x(t_0)||) + \frac{c}{\lambda}, \tag{5}
\end{align*}
\]
where \( c = \max_{i \in I} \{ c_i \}, \alpha = \alpha + \phi_2 \). From (5), for any bounded initial conditions \( x_0 \in \Omega \), there exists a compact set \( \Omega_{x} = \{ x| ||x|| \leq \phi_1^{-1}\left( \bar{\sigma}(||x(t_0)||) + \frac{c}{\lambda} \right) \} \) such that for all \( t_0 \geq 0 \), \( x(t) \in \Omega_x \).

(1) When \( V_{\xi}(x(t_0)) - \frac{c}{\lambda} + \alpha(||x(t_0)||) = 0 \), for any bounded initial conditions \( x_0 \in \Omega \), (5) implies that \( \lim_{t \to \infty} ||x(t)|| = \phi_1^{-1}\left( \frac{c}{\lambda} \right) \), i.e., there is \( T > 0 \) such that state \( x(t) \in \Omega_x = \{ x| ||x|| \leq \phi_1^{-1}\left( \frac{c}{\lambda} \right) \}, t \geq T \).

(2) When \( V_{\xi}(x(t_0)) - \frac{c}{\lambda} + \alpha(||x(t_0)||) \neq 0 \), for any \( x_0 \in \Omega \), we have \( \lim_{t \to \infty} ||x(t)|| = \phi_1^{-1}\left( \frac{c}{\lambda} \right) \).

Therefore, the closed-loop system is semiglobally uniformly ultimately bounded.

**B. PROBLEM FORMULATION**

1) **SYSTEM DESCRIPTION**

Consider system (1) in the special form
\[
\begin{align*}
\dot{x} &= f_{\sigma}(z, x_1), \\
\dot{x}_1 &= x_2 + f_{\sigma}(z, \tilde{x}_1), \\
\dot{x}_2 &= x_3 + f_{\sigma}(z, \tilde{x}_2), \\
&\vdots \\
\dot{x}_{n-1} &= x_n + f_{(n-1)\sigma}(z, \tilde{x}_{n-1}), \\
\dot{x}_n &= u_t + f_{\sigma}(z, \tilde{x}_n), \\
y &= x_1,
\end{align*}
\]
where \( z \in \mathbb{R}^p, x = (x_1, x_2, \ldots, x_n)^T \) are the system states with \( \tilde{x}_k = (x_1, \ldots, x_k)^T, k = 1, 2, \ldots, n \), \( i \in I \) are unknown smooth functions and \( f_{i}(0) = 0 \), \( f_{k}(0) = 0, k = 1, 2, \ldots, n, i \in I \) are continuous functions satisfying \( \psi_i(0) = 0 \) and \( y^T \psi_i(0) \geq 0 \).

In this paper, for a given reference signal \( y_{d}(t) \), the main control objective is to design adaptive NNs-based controller for each subsystem of system (7) and an appropriate switching law such that

(a) all the signals of the resulting closed-loop system are semiglobally uniformly ultimately bounded,

(b) the output of the system can follow the reference signal \( y_{d}(t) \) to a small compact.

To this end, we make the following assumptions.

**Assumption 1:** There exists a positive definite and radially unbounded smooth function \( W_i(z) \), \( \beta_{ij}(z) \leq 0 \), and smooth functions \( \mu_{ij}(z) \) with \( \mu_{ij}(0) = 0 \) and \( \mu_{ii}(z) = 0, \) constants \( c_i \geq 0, \lambda_i > 0 \) for \( i, j \in I \) such that
\[
\begin{align*}
L_{ij}^o(z, x_d) &= \gamma_i W_i(z) + \lambda_i W_i(z) \tag{9}
\end{align*}
\]
\[
\begin{align*}
&\quad + \sum_{k=1}^{M} \beta_{ik}(z) (W_i(z) - W_k(z) + \mu_{ik}(z)) \leq c_i \tag{10}
\end{align*}
\]
\[
\begin{align*}
&\quad \mu_{ij}(z) + \mu_{jk}(z) \leq \min \{0, \mu_{ik}(z)\} \quad \text{hold for } i, j \in I.
\end{align*}
\]
Assumption 2: The reference signal $y_d(t)$ and its time derivatives $\dot{y}_d(t), \ddot{y}_d(t), \ldots, \dot{y}_d^{(n)}(t)$ are continuous and bounded.

Remark 2: Under Assumption 1, the tracking control problem for each subsystem is not required to be solvable. Therefore, Assumption 1 is much weaker than the conditions provided in [23], [26], [30]. Assumption 1 can degenerate into [30] by letting $\epsilon_1 = 0$.

2) FUNCTION APPROXIMATION USING RBF NNs

RBF neural network is usually used to model nonlinear functions. In [35], an unknown continuous function $f(\mathbf{X}): R^n \rightarrow R$ can be expressed as $f(\mathbf{X}) = \hat{W}\mathbf{s}(\mathbf{X}) + \varepsilon(\mathbf{X})$, where $\mathbf{X} = [x_1, \ldots, x_n]^T \in R^n$ is the input vector of NNs, $\hat{W} \in R^l$ is a weight vector of the NN, $l > 1$ is the number of the NN nodes, $\varepsilon(\mathbf{X})$ is the approximation error which satisfies $|\varepsilon(\mathbf{X})| \leq |\varepsilon|$ and $\varepsilon$ is an unknown bounded parameter, $\mathbf{S}(\mathbf{X}) = [s_1(\mathbf{X}), \ldots, s_l(\mathbf{X})]^T \in R^l$ is the basis function vector, where $s_i(\mathbf{X})$ can be chosen as the Gaussian functions in th form

$${s_i(\mathbf{X}) = \exp \left[\frac{-(\mathbf{X} - \mu_i)^T(\mathbf{X} - \mu_i)}{\xi_i^2}\right], \quad i = 1, 2, \ldots, l,} \tag{12}$$

where $\mu_i = [\mu_{i1}, \mu_{i2}, \ldots, \mu_{in}]^T$ is the center of the receptive field and $\xi_i$ is the width of the Gaussian function.

As mentioned in [36], for sufficiently large nodes number $l$, the RBF neural networks $\theta^* \mathbf{S}(\mathbf{X})$ can approximate any continuous function $f(\mathbf{X})$ over a compact set $\Omega$, that is, for $\forall \varepsilon > 0$, there exists the RBF neural networks $W^* \mathbf{S}(\mathbf{X})$ such that

$$f(\mathbf{X}) = \theta^* \mathbf{S}(\mathbf{X}) + \varepsilon^* (\mathbf{X}), \quad \forall \mathbf{X} \in \Omega \subset R^n, \tag{13}$$

where $W^*$ is the optimal weight and $|\varepsilon^* (\mathbf{X})| \leq \varepsilon$ is the smallest approximation error.

III. MAIN RESULTS

This section will solve the output tracking control problem of system (7) using the exponential quasi-passivity concept.

A. NEURAL NETWORKS-BASED ADAPTIVE EXPONENTIAL QUASI-PASSIFICATION CONTROLLER AND SWITCHING LAW DESIGN

In the following, a set of adaptive controllers and a state-dependent switching law will be designed constructively to solve the exponential quasi-passification problem of system (7).

Step 1: Consider the $i$-th $(z, x_1)$ subsystem. Construct the output $e_1 = x_1 - y_d$. Thus, the $i$-th $(z, x_1)$ subsystem is described by

$$\begin{align*}
\dot{z} &= f_{0i}(z, e_1 + y_d), \\
\dot{e}_1 &= x_2 + f_{1i}(z, e_1 + y_d) - \dot{y}_d,
\end{align*} \tag{14}$$

where $x_2$ is a virtual input of (14). Thus, the zero dynamics of system (14) is $\ddot{z} = f_{0i}(z, y_d)$. Using the mean value theorem gives:

$$f_{0i}(z, e_1 + y_d) = f_{0i}(z, y_d) + e_1^T \frac{\partial f_{0i}(z, e_1 + y_d)}{\partial e_1} \frac{\partial f_{0i}(z, e_1 + y_d)}{\partial e_1} ds$$

where $\frac{\partial f_{0i}(z, e_1 + y_d)}{\partial e_1} = \int f_{0i} \frac{\partial f_{0i}(z, e_1 + y_d)}{\partial e_1} \frac{\partial f_{0i}(z, e_1 + y_d)}{\partial e_1} ds$ are unknown smooth functions. Let

$$R_{1i}(X_1) = f_{1i}(z, x_1) + \frac{1}{l} \frac{\partial W_i}{\partial z} f_{0i}(z, x_1) - \dot{y}_d,$$

$$X_1 = (z, x_1, y_d, \dot{y}_d).$$

Using an RBF neural network $\hat{\theta}_{i1}^* S_1(X_1) + \varepsilon_{i1}^*$ to approximate $R_{1i}(X_1)$ gives

$$R_{1i}(X_1) = \hat{\theta}_{i1}^* S_1(X_1) + \varepsilon_{i1}^*(X_1), \quad |\varepsilon_{i1}^*| \leq \bar{\varepsilon}_1$$

with the ideal constant weights $\hat{\theta}_{i1}^*$, and the approximation error $\varepsilon_{i1}^*$. Define an unknown constant $\Theta_1 = \max \{||\theta_{i1}||^2\}$. A storage function for system (14) is constructed as

$$V_{1i}(z, e_1, \hat{\Theta}_1) = \frac{1}{2} W_i(z) + \frac{e_1^2}{2} + \frac{1}{2l} \hat{\Theta}_1 \hat{\Theta}_1$$

with the estimation error $\hat{\Theta}_1 = \Theta_1 - \hat{\Theta}_1$, where $\hat{\Theta}_1$ is the estimation of $\Theta_1, l > 0$ is a design parameter.

Differentiating $V_{1i}$ together with (9) gives

$$\dot{V}_{1i} = e_1 \left( x_2 + \frac{1}{l} \frac{\partial W_i}{\partial z} f_{0i}(z, e_1 + y_d) + f_{1i}(z, e_1 + y_d) - \dot{y}_d \right)$$

$$\dot{e}_1 = \frac{1}{l} \frac{\partial W_i}{\partial z} f_{0i}(z, y_d) - \frac{1}{l} \hat{\Theta}_1 \hat{\Theta}_1$$

Applying the Young’s inequality gives

$$e_1 \varepsilon_{i1}^* S_1(X_1) \leq \frac{e_1^2}{2a_1} \hat{\Theta}_1 S_1^T S_1 + \frac{a_1^2}{2} e_1 \varepsilon_{i1}^* \leq \frac{e_1^2}{2} + \frac{\bar{\varepsilon}_1^2}{2}. \tag{17}$$

where $a_1 > 0$ is a design parameter. Therefore,

$$\dot{V}_{1i} \leq e_1 \left( x_2 + \frac{1}{2a_1} \hat{\Theta}_1 S_1^T S_1 + \frac{e_1^2}{2} \right) + \frac{a_1^2}{2}$$

$$\leq \frac{e_1^2}{2a_1} \hat{\Theta}_1 S_1^T S_1 - \lambda \hat{\Theta}_1, \tag{18}$$

Design the virtual common controller as:

$$\begin{align*}
x_2 &= a_1 (\hat{\Theta}_1, e_1, X_1) + e_2, \\
a_1 &= -\frac{e_1}{2a_1} \hat{\Theta}_1 S_1^T S_1 - \left( \frac{\lambda}{2} + \frac{1}{2} \right) e_1 + \dot{y}_d, \\
\hat{\Theta}_1 &= l \frac{e_1}{2a_1} S_1^T S_1 - \lambda \hat{\Theta}_1, \tag{19}
\end{align*}$$

where $\lambda = \min \{\lambda_i\}$. From (9) and (19), we have

$$\dot{V}_{1i} \leq e_1 e_2 - \lambda \frac{e_1^2}{2} + \frac{a_1^2}{2} + \bar{\varepsilon}_1^2$$

$$\leq e_1 e_2 - \lambda \frac{e_1^2}{2} + \frac{a_1^2}{2} + \frac{\bar{\varepsilon}_1^2}{2}$$
\[\begin{align*}
&\leq e_1 e_2 -\frac{\lambda}{T} W_1 (z) - \frac{e_1^2}{2} - \frac{\lambda}{2} \Theta_1^2 + \frac{a_1^2}{2} + \frac{\lambda}{2} \Theta_2^2 + \frac{\varepsilon_1^2}{2} + \frac{\lambda}{2} \Theta_3^2 + \frac{a_2}{2} + \frac{\lambda}{2} \Theta_4^2 + \frac{\varepsilon_2}{2} + \frac{\lambda}{2} \Theta_5^2 \\
+ &\sum_{k=1}^{M} \beta_{ik} (z) \left( W_i (z) - W_k (z) \right) + \frac{\mu_{ik} (z)}{l} + c_i \\
&\leq e_1 e_2 -\lambda V_{1i} + \frac{a_1^2}{2} + \frac{\varepsilon_1^2}{2} + \frac{\lambda}{2} \Theta_2^2 + \frac{\lambda}{2} \Theta_3^2 + \frac{\lambda}{2} \Theta_4^2 + \frac{\varepsilon_2}{2} + \frac{\lambda}{2} \Theta_5^2 + \frac{a_2}{2} + \frac{\lambda}{2} \Theta_6^2 + \frac{\varepsilon_3}{2} + \frac{\lambda}{2} \Theta_7^2 \\
+ &\sum_{k=1}^{M} \beta_{ik} (z) (V_{1i} (z, e_i) - V_k (z, e_i)) + \bar{\mu}_{ik} (z, e_i),
\end{align*}\]

where \(\bar{\mu}_{ik} (z, e_i) = \frac{1}{2} \mu_{ik} (z)\).

Step \(j (1 \leq j \leq n-1)\): Let \(X_k = (z, \bar{x}, \Theta_1, \ldots, \Theta_{j-1}, y_d, \ldots, y_d^{(k)})\), \(Z_j = (z, e_1, \ldots, e_j)\), \(\theta_j = (\Theta_1, \ldots, \Theta_j)\). Repeating this process, we can obtain, at the \(j\)-th step, that the virtual output, virtual input, and storage functions of \((z, x_1, \Theta_1, \ldots, \Theta_{j-1})\) subsystem: \(e_{j-1} = x_{j-1} - \alpha_j\) and \(x_j = \alpha_j (X_j) + e_j\), \(V_{j-1,i} (Z_{j-1}, \theta_{j-1}) = \frac{1}{2} W_i (z) + \sum_{k=1}^{j-1} \frac{a_k^2}{2} + \frac{\varepsilon_k^2}{2} + \frac{\lambda}{2} \Theta_k^2 + c_k\) satisfying

\[\begin{align*}
\dot{V}_{j-1,i} &\leq e_{j-1} e_j - \lambda V_{j-1,i} + \frac{1}{2} \sum_{k=1}^{j-1} \left( \frac{a_k^2}{2} + \frac{\varepsilon_k^2}{2} + \frac{\lambda}{2} \Theta_k^2 + c_k \right) \\
+ &\sum_{k=1}^{M} \beta_{ik} (z) \left( V_{j-1,i} (Z_{j-1}, \theta_{j-1}) - V_{j-1,k} (Z_{j-1}, \theta_{j-1}) \right) \\
+ &\bar{\mu}_{ik} (Z_{j-1}, \theta_{j-1}).
\end{align*}\]

(20)

where \(\bar{\mu}_{ik} = \frac{1}{2} \mu_{ik} (z)\).

Consider the \(i\)-th \((z, \bar{x}, \Theta_1, \ldots, \Theta_{j-1})\) subsystem. Let the output \(e_j = x_j - \alpha_{j-1} \dot{x}_{j-1}\) is a virtual input of \(i\)th \((z, \bar{x}, \Theta_1, \ldots, \Theta_{j-1})\) subsystem. Let \(R_{i,i} (X_j) = f_{i,i} (z, \bar{x}) - \dot{\alpha}_{j-1}\), which are the unknown functions. Employing an RBF neural network \(\hat{\theta}_{i,j}^* S_j (X_j)\) to approximate \(R_{i,i} (X_j)\) gives

\[\begin{align*}
R_{i,i} (X_j) = \theta_{i,j}^* S_j (X_j) + e_{i,j} (X_j),
\end{align*}\]

where \(\hat{\theta}_{i,j}^*\) denotes the ideal constant weights, \(e_{i,j}\) is the approximation error with constant \(\tilde{e}_j > 0\). Define \(\Theta_j = \max_{i \in I} \left\{ \| \theta_{ij} \|^2 \right\}\).

Choose the storage function as

\[\begin{align*}
V_{ji} (z_j, \theta_j) = &\ V_{j-1,i} (Z_{j-1}, \theta_{j-1}) + \frac{\varepsilon_j^2}{2} + \frac{\Theta_j^2}{2T},
\end{align*}\]

where \(\bar{\Theta}_j = \Theta_j - \hat{\Theta}_j, \hat{\Theta}_j\) is the estimation of \(\Theta_j\).

The derivative of \(V_{ji}\) along the trajectory of the \(i\)-th \((z, \bar{x}, \Theta_1, \ldots, \Theta_{j-1})\) subsystem together with (20) and (21) is

\[\begin{align*}
\dot{V}_{ji} &\leq (e_{j-1} + x_{j+1} + f_{i,i} (z, \bar{x}) - \dot{\alpha}_j) e_j - \lambda V_{j-1,i} + \sum_{k=1}^{j-1} \frac{a_k^2}{2} + \frac{\varepsilon_k^2}{2} + \frac{\lambda}{2} \Theta_k^2 + c_k \Theta_j - \hat{\Theta}_j \\
+ &\sum_{k=1}^{M} \beta_{ik} (z) \left( V_{ji} (Z_j, \theta_j) - V_{jk} (Z_j, \theta_j) + \bar{\mu}_{ik} \right) + \tilde{e}_j^2.
\end{align*}\]

Applying the Young’s inequality gives

\[\begin{align*}
e_{i,j} \theta_{i,j}^* S_j (X_j) &\leq \frac{\varepsilon_j^2}{2T} \Theta_j S_j (X_j) + \frac{a_k^2}{2} + \frac{\varepsilon_k^2}{2} + \frac{\lambda}{2} \Theta_k^2 + c_k, \quad e_{i,j} \leq \frac{\varepsilon_j}{2} + \frac{\Theta_k^2}{2T} + \frac{\varepsilon_k}{2},
\end{align*}\]

where \(a_{j+1} > 0\) is a design parameter.

Design the virtual common controller as:

\[\begin{align*}
x_{j+1} = \alpha_j + e_{j+1},
\end{align*}\]

\[\begin{align*}
\alpha_j = -\frac{e_j}{2a_j} \hat{\Theta}_j S_j (X_j) - e_{j-1} - \frac{\lambda}{2} e_j, \quad \hat{\Theta}_j = \frac{\Theta_j}{2a_j} S_j (X_j) - \lambda \hat{\Theta}_j.
\end{align*}\]

(24)

Substituting (23), (24) into (22) gives

\[\begin{align*}
\dot{V}_{j,i} &\leq e_{i,j} e_j + \frac{a_k^2}{2} + \frac{\varepsilon_k^2}{2} + \frac{\lambda}{2} \Theta_k^2 + c_k \Theta_j - \hat{\Theta}_j \\
+ &\sum_{k=1}^{M} \beta_{ik} (z) \left( V_{j,i} (Z_j, \theta_j) - V_{j,k} (Z_j, \theta_j) + \bar{\mu}_{ik} \right).
\end{align*}\]

(25)

Step \(n\): According to the above analysis, we have

\[\begin{align*}
\dot{V}_{n-1,i} &\leq e_{n-1} e_n - \lambda V_{n-1,i} + \frac{a_k^2}{2} + \frac{\varepsilon_k^2}{2} + \frac{\lambda}{2} \Theta_k^2 + c_k \Theta_j - \hat{\Theta}_j \\
+ &\sum_{k=1}^{M} \beta_{ik} (z) \left( V_{n-1,i} (Z_{n-1}, \theta_{n-1}) - V_{n-1,k} (Z_{n-1}, \theta_{n-1}) + \bar{\mu}_{ik} \right).
\end{align*}\]

Consider the \(i\)-th \((z, \bar{x}, \Theta_1, \ldots, \Theta_{n-1})\) subsystem. Define the output \(e_n = x_n - \alpha_{n-1}\). Use an RBF neural network \(\theta_{n,i}^* S_n (X_n)\) to approximate \(f_{n,i} (z, \bar{x}) - \alpha_{n-1}\).

Let \(\Theta_{j,n} = \max_{i \in I} \left\{ \| \theta_{ij,n} \|^2 \right\}\). Choose the storage function as

\[\begin{align*}
V_{ni} (Z_n, \theta_n) = V_{n-1,i} (Z_{n-1}, \theta_{n-1}) + \frac{\varepsilon_j^2}{2} + \frac{\Theta_j^2}{2T},
\end{align*}\]

where \(\bar{\Theta}_n = \Theta_n - \hat{\Theta}_n\) and \(\hat{\Theta}_n\) is the estimation of \(\Theta_n\). Design the controllers as:

\[\begin{align*}
\alpha_n = -\frac{e_n}{2a_n} \hat{\Theta}_n S_n (X_n) - e_{n-1} - \frac{\lambda}{2} e_n, \\
\dot{\hat{\Theta}_n} = \frac{\Theta_n}{2a_n} S_n (X_n) - \lambda \hat{\Theta}_n.
\end{align*}\]
The derivative of $V_{nl}$ is
\[
\dot{V}_{nl} \leq e_n v_i - \lambda V_{nl} + \sum_{k=1}^{M} \left( \frac{a_k^2}{2} + \frac{\sigma_i^2}{2} + \frac{\lambda}{l} \Theta_i^2 \right) + c_i
\]
\[
+ \sum_{k=1}^{M} \tilde{P}_{ik} (Z_n, \vartheta_n) (V_{nl} (Z_n, \vartheta_n) - V_{nk} (Z_n, \vartheta_n) + \tilde{P}_{ik} (Z_n, \vartheta_n))
\]
\[
+ \mu_{ik} (Z_n, \vartheta_n),
\]
(27)
where $\tilde{P}_{ik} (Z_n, \vartheta_n) = \beta_{ik} (\sigma) \cdot \mu (Z_n, \vartheta_n) = \frac{1}{l} \mu_{ik} (\sigma)$.

Let
\[
\Omega_i = \{ (Z_n, \vartheta_n) | V_{nl} (Z_n, \vartheta_n) - V_{nk} (Z_n, \vartheta_n) + \mu_{ik} (Z_n, \vartheta_n) \leq 0, j \in I \}
\]
and
\[
\tilde{\Omega}_{ij} = \{ (Z_n, \vartheta_n) | V_{nl} (Z_n, \vartheta_n) - V_{nk} (Z_n, \vartheta_n) + \tilde{P}_{ik} (Z_n, \vartheta_n) = 0, i \neq k \}.
\]

According to [22], the set $\{ \Omega_i | i \in I \}$ is a partition of $R^{2n+lp}$. When $V_{nl} (Z_n, \vartheta_n) - V_{nk} (Z_n, \vartheta_n) + \mu_{ik} (Z_n, \vartheta_n) \leq 0$, we have
\[
\dot{V}_{nl} \leq e_n v_i - \lambda V_{nl} + \sum_{k=1}^{n} \left( \frac{a_k^2}{2} + \frac{\sigma_i^2}{2} + \frac{\lambda}{l} \Theta_i^2 \right) + c_i.
\]
(28)

Multiplying both sides of (28) by $e^{\lambda t}$, respectively, yields:
\[
\frac{d}{dt} (e^{\lambda t} V_{nl}) \leq e^{\lambda t} (e_n v_i + C_i),
\]
(29)
where $C_i = \sum_{k=1}^{n} \left( \frac{a_k^2}{2} + \frac{\sigma_i^2}{2} + \frac{\lambda}{l} \Theta_i^2 \right) + c_i$.

Integrating (29) over $[s, t]$ for $s \geq t_0$ gives:
\[
e^{\lambda t} V_{nl}(t) - e^{\lambda s} V_{nl}(s) \leq \int_{s}^{t} e^{\lambda \tau} (e_n (\tau) v_i(\tau) + C_i) d\tau.
\]
(30)

Design the switching law as:
\[
\sigma (t) = i \text{ if } \sigma (t^-) = i \text{ and } x (t) \in \Omega_i.
\]
\[
\sigma (t) = \min \left\{ j | x (t) \in \tilde{\Omega}_{ij} \right\} \text{ if } \sigma (t^-) = i \text{ and } x (t) \in \tilde{\Omega}_{ij}.
\]
(31)

From (31), we have
\[
V_{nl} (Z_n (t), \vartheta_n (t)) - V_{nk} (Z_n (t), \vartheta_n (t)) = \mu_{ik} (Z_n (t), \vartheta_n (t)), \quad l = 0, 1, \ldots
\]
(32)
and $e^{\lambda t} \mu_{ik} (Z_n (t), \vartheta_n (t))$ are decreasing on $[t_1, t_{l+1})$.

The storage function of system (7) is defined as $V (\vartheta (t), Z_n, \vartheta_n) = V_{\sigma(t)} (Z_n, \vartheta_n)$. For $t \geq t_0 > 0$ and $t \in \{t_k, t_{k+1}\}$.

From (30), (32), and (21), we have:
\[
e^{\lambda t} V (\vartheta (t), Z_n (t), \vartheta_n (t)) - e^{\lambda t} V (\vartheta (t_0), Z_n (t_0), \vartheta_n (t_0)) = e^{\lambda t} V_{ik} (Z_n (t), \vartheta_n (t)) - e^{\lambda t} V_{ik} (Z_n (t_0), \vartheta_n (t))
\]
\[
+ \sum_{p=0}^{k-1} e^{\lambda t} V_{lp} (Z_n (t_{p+1}), \vartheta_n (t_{p+1}))
\]
\[
- e^{\lambda t} V_{lp} (Z_n (t_p), \vartheta_n (t_p))
\]
\[
+ \sum_{p=1}^{k} e^{\lambda t} (V_{lp} (Z_n (t_p), \vartheta_n (t_p)) - V_{lp} (Z_n (t_{p-1}), \vartheta_n (t_{p-1})))
\]
\[
- V_{l_{p-1}} (Z_n (t_{p-1}), \vartheta_n (t_{p-1})))
\]
\[
\leq \int_{t_0}^{t} e^{\lambda \tau} (e_n (\tau) v_\sigma (\tau) + C_\sigma) d\tau
\]
\[
+ \sum_{p=1}^{k} e^{\lambda t} (V_{lp} (Z_n (t_p), \vartheta_n (t_p)) - V_{lp} (Z_n (t_{p-1}), \vartheta_n (t_{p-1})))
\]
\[
\leq \int_{t_0}^{t} e^{\lambda \tau} (e_n (\tau) v_\sigma (\tau) + C_\sigma) d\tau
\]
\[
+ \sum_{p=1}^{k} e^{\lambda t} (V_{lp} (Z_n (t_p), \vartheta_n (t_p)) - V_{lp} (Z_n (t_{p-1}), \vartheta_n (t_{p-1})))
\]
\[
\leq \int_{t_0}^{t} e^{\lambda \tau} (e_n (\tau) v_\sigma (\tau) + C_\sigma) d\tau
\]
\[
+ e^{\lambda t} \alpha (\{ (Z_n (t_0), \vartheta_n (t_0)) \})
\]
(33)
where $\alpha (s) = \max \{ \mu_{ik} (Z_n, \vartheta_n) | i, k \in I \}$ is a class $\mathcal{K}$ function. Therefore, system (7) is exponentially quasi-passive.

**Remark 3:** Because of the existence of uncertainty, quasi-passification was only achieved instead of exact feedback passification.

**B. STABILITY ANALYSIS**

Based on the above quasi-passive system, the output tracking problem will be solved by output feedback controllers.

**Theorem 1:** Consider system (7). For the given reference signal $y_d (t)$, suppose Assumptions 1,2 hold. Then, there exists the switching law (31) and adaptive controllers (26) such that closed-loop system is exponentially quasi-passive from the inputs $v_j$ to the output $e_n = x_n - a_n$. Furthermore, if the new control input is redesigned as $\bar{v}_i = -\Psi_i (e_n)$ with the continuous function $\Phi_i (\cdot)$ satisfying $e^\lambda \Psi_i (e_n) \geq 0$, the output tracking control problem is solvable.

**Proof:** By Lemma 1, all the signals of the resulting closed-loop system are semiglobally uniformly ultimately bounded. Thus, all the signals $\{ z, e_1, \ldots, e_n, \Theta_1, \ldots, \Theta_n \}$ in the closed-loop system are bounded. Because $\Theta_1, \Theta_2 \ldots \Theta_n$ are constants, $\tilde{\Theta}_1, \ldots, \tilde{\Theta}_n$ are bounded. By Assumption 2, $z, x_1, \ldots, x_n$ are bounded. The states and parameter estimation errors converge to compact sets whose sizes can be reduced by choosing appropriate design parameters $l$ and $a_i$. On the other hand, for all initial condition, $e_1$ eventually converges to the compact set. Therefore, the output can follow the reference signal $y_d (t)$ in a small compact.

**Remark 4:** In contrast to conventional backstepping, a class of nonlinear adaptive controllers with new control inputs are designed constructively. The new control inputs can be redesigned to solve the tracking and stabilization problem and so on. The switching law (31) can degenerate into the well-known “min-switching” law in [23] by setting $\mu_{ij} \equiv 0$. 

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IV. EXAMPLE

In this section, a numerical example is given to demonstrate the effectiveness of the results.

Consider the following system

\[
\begin{aligned}
\dot{z} &= f_0(z, x_1), \\
\dot{x}_1 &= x_2 + f_1(z, \tilde{x}_1), \\
\dot{x}_2 &= u + f_2(z, \tilde{x}_2),
\end{aligned}
\]

where \( \sigma(t) : [0, +\infty) \to I = [1, 2] \) and \( \sigma(z_1, z_2) : [z_1, z_2]^T \in \mathbb{R}^2 \), \( x = [x_1, x_2]^T \in \mathbb{R}^2 \), \( f_0 = [-9z_1 + 3x_1, 2z_2 + \cos(z_1z_2)]^T \), and \( f_1, f_2 = \) as described in Fig. 4. Figs. 2 and 3 imply the outputs of the system (33) are solvable by the controllers and update laws as:

\[
\begin{aligned}
x_2 &= \cos t - \frac{e_1}{2\alpha_1} \tilde{\Theta}_1 S_1 \sigma(z_1, z_2) - \left( \frac{\lambda_1}{2} + \frac{1}{2} \right) e_1 + e_2, \\
u_1 &= -\frac{e_2}{2\alpha_2} \tilde{\Theta}_2 S_2 e_1 - \frac{\lambda_1}{2} e_2 + v_1, \\
u_2 &= -\frac{e_2}{2\alpha_2} \tilde{\Theta}_2 S_2 e_1 - \frac{\lambda_2}{2} e_2 + v_1,
\end{aligned}
\]

where \( \lambda = \min \{\lambda_i | i = 1, 2\} = 1. \)

Design the switching law as follows:

\[
\begin{aligned}
\dot{\tilde{e}}_1 &= \frac{e_2}{2} - \frac{\lambda_1}{2} \tilde{\Theta}_1, \\
\dot{\tilde{e}}_2 &= \frac{e_2}{2} - \frac{\lambda_2}{2} \tilde{\Theta}_2, \\
V_{21} &= V_{li} + \frac{e_2^2}{2} + \frac{1}{2} \tilde{\Theta}_2, \\
V_{l1} &= \frac{1}{l} W_{li} (z) + \frac{e_2^2}{2} + \frac{1}{2l} \tilde{\Theta}_1^2, \\
\end{aligned}
\]

where \( \alpha_i = 0.24, \alpha_2 = 0.2, l = 20 \).

The input vectors of RBFNNs are \( X_1 = (z_1, z_2, x_1, y_d, \dot{y}_d) \) and \( X_2 = \left( z_1, z_2, \tilde{\Theta}_1, \ldots, \tilde{\Theta}_{k-1}, y_d, \ldots, y_d^{(k)} \right)^T \). The centers and widths are chosen on a regular lattice in the respective compact sets. The centers and widths of RBFNNs are spaced on \([-2, 2], [-2, 2], \ldots, [-2, 2]\). The widths of RBFNNs are \( \xi_1 = \xi_2 = 2 \). The simulation was performed with the initial state \( z(0), x(0) = (-1.5, 0.6, -0.2, -0.05) \), \( \tilde{\Theta}_1(0) = 0, \tilde{\Theta}_2(0) = 0 \).

The simulation results are shown in Figs. 1-4. See from Figure 1, the states are bounded under the switching law described in Fig. 4. Figs. 2 and 3 imply the outputs of the system (33) can track the reference signal under the controllers.
as shown in Fig. 5. Therefore, the adaptive tracking control problem of the resulting closed-loop system (33) - (39) is solvable. The simulation results well illustrate the effectiveness of the proposed approach.

V. CONCLUSION

This paper has studied adaptive exponential quasi-passification and adaptive tracking control for uncertain switched nonlinear systems in lower-triangular form. A more general switching law and adaptive controller are designed constructively. There are relevant problems that need to be investigated. One of such problems is how to solve finite time tracking problems using finite-time quasi-passivity for switched nonlinear systems.

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