Synthesis and Polymorphism of Mixed Aluminium-Gallium Oxides

Daniel S. Cook,¹ Joseph E. Hooper,² Daniel M. Dawson,² Janet M. Fisher,³ David Thompsett,³ Sharon E. Ashbrook²* and Richard I. Walton¹*

1. Department of Chemistry, University of Warwick, Coventry, CV4 7AL, UK
2. School of Chemistry, EaStCHEM and Centre of Magnetic Resonance, University of St Andrews, North Haugh, St Andrews, KY16 9ST, UK
3. Johnson Matthey Technology Centre, Sonning Common, Reading, RG4 9NH, UK

* Authors for correspondence: Email: r.i.walton@warwick.ac.uk and sema@st-andrews.ac.uk

Abstract

The synthesis of a new solid solution of the oxyhydroxide Ga₅-xAlₓO₇(OH) is investigated via solvothermal reaction between gallium acetylacetonate and aluminium isopropoxide in 1,4-butaneol at 240 °C. A limited compositional range 0 ≤ x ≤ 1.5 is produced, with the hexagonal unit cell parameters refined from powder X-ray diffraction (XRD) showing a linear contraction in unit cell volume with increasing Al content. Solid-state ²⁷Al and ⁷¹Ga NMR spectroscopy show a strong preference for Ga to occupy the tetrahedral sites and Al to occupy the octahedral sites. Using isopropanol as the solvent, γ-Ga₂₋ₓAlₓO₃ defect spinel solid solutions with x ≤ 1.8 can be prepared at 240 °C in 24 hours. These materials are nanocrystalline, as evidenced by their broad diffraction profiles, but the refined cubic lattice parameter shows a linear relationship with the Ga:Al content and solid-state NMR spectroscopy again shows a preference for Al to occupy the octahedral sites. Thermal decomposition of the Ga₅₋ₓAlₓO₇(OH) occurs via poorly ordered materials that resemble ε-Ga₂₋ₓAlₓO₃ and κ-Ga₂₋ₓAlₓO₃, but γ-Ga₂₋ₓAlₓO₃ transforms above 750 °C to monoclinic β-Ga₂₋ₓAlₓO₃ for 0 ≤ x ≤ 1.3 and to hexagonal α-Ga₂₋ₓAlₓO₃ for x = 1.8, with intermediate compositions 1.3 < x < 1.8 giving mixtures of the α and β polymorphs. Solid-state NMR spectroscopy shows only the expected octahedral Al for α-Ga₂₋ₓAlₓO₃ and, for β-Ga₂₋ₓAlₓO₃, the ~1:2 ratio of tetrahedral:octahedral Al is in good agreement with Rietveld analysis of the average structures against powder XRD data. Relative energies calculated by periodic density functional theory (DFT) confirm that there is a ~5.2 kJ mol⁻¹ penalty for tetrahedral rather than octahedral Al in Ga₅₋ₓAlₓO₇(OH), whereas this penalty is much lower (~2.0 kJ mol⁻¹) for β-Ga₂₋ₓAlₓO₃, in good qualitative agreement with the experimental NMR spectra.
Introduction

Polymorphism in the Al-O, Al-(OH) and Al-O-(OH) systems is well established and has been researched extensively, in part owing to the huge importance of aluminium oxide polymorphs as supports for precious metals and other reactive species in many areas of catalysis.\textsuperscript{1-2} Alumina polymorphs (in particular $\gamma$-Al$_2$O$_3$) are not only used as catalyst supports but also as adsorbents, coatings, soft abrasives or as catalysts themselves, owing to their typically high surface areas and surface activity.\textsuperscript{3} At least 11 oxides, hydroxides and oxyhydroxides of aluminium are known.\textsuperscript{1} The thermodynamically stable polymorph of alumina, at room temperature and pressure, is $\alpha$-Al$_2$O$_3$ (corundum), and all metastable aluminas, commonly referred to in industry as transition aluminas, convert to this polymorph at sufficiently high temperature.

Gallium oxide polymorphism had received comparatively little focus until the past 5 years, when an interest in the electronic properties of various forms of the materials has attracted growing attention;\textsuperscript{4} in particular, in microelectronics where the large bandgap of $\beta$-Ga$_2$O$_3$ offers new possibilities in high-frequency power devices,\textsuperscript{5} but also in photocatalysis where mixtures of polymorphs can lead to cooperative behaviour at phase junctions.\textsuperscript{6-7} Much of the previous understanding of the structures of gallium oxide polymorphs stemmed from the work of Roy and co-workers in the 1950s\textsuperscript{8-9} and, until recently, the polymorphism in the Ga-O, Ga-(OH) and Ga-O-(OH) systems remained poorly characterised despite a large number of publications on the structural characterisation of gallium oxide.\textsuperscript{10-14} The recent work of some of us clarified the structures of a number of gallium oxide polymorphs, some of which contain inherent structural disorder leading to poor crystallinity.\textsuperscript{15-16} The thermodynamically stable polymorph under ambient conditions is the monoclinic $\beta$ polymorph (in contrast to the $\alpha$ polymorph for aluminium oxide) whose structure contains a 1:1 ratio of octahedral: tetrahedral cations, both in distorted coordination geometry.\textsuperscript{17} $\alpha$-Ga$_2$O$_3$, structurally analogous to $\alpha$-Al$_2$O$_3$, is metastable but $\beta$-Ga$_2$O$_3$ irreversibly converts to this polymorph at high pressure because $\alpha$-Ga$_2$O$_3$ has a smaller molar volume.\textsuperscript{18} The cation-defective spinel $\gamma$-Ga$_2$O$_3$ can be prepared directly by oxidation of gallium
metal in an aminoalcohol.\textsuperscript{15-16} \( \gamma \)-Ga\textsubscript{2}O\textsubscript{3} is structurally analogous to \( \gamma \)-Al\textsubscript{2}O\textsubscript{3},\textsuperscript{20} both having disordered spinel structures containing small amounts of cations occupying non-spinel sites in the unit cell, yet allowed in the \( Fd\bar{3}m \) space group.\textsuperscript{16} Other less well-characterised forms of Ga\textsubscript{2}O\textsubscript{3} include the \( \varepsilon \) and \( \kappa \) polymorphs, whose preparation is complicated by their transient nature during thermal decompositions of other gallium oxides or oxyhydroxides.\textsuperscript{15}

Given the present interest in the electronic properties of gallium oxides, it is timely to consider the polymorphism of solid solutions of gallium and aluminium oxides. As noted above, although the two binary oxide systems show similarities in the types of structures adopted, they show different relative stabilities and, in fact, are accessed by different synthesis approaches. The greater preference of tetrahedral coordination by gallium is of note and this could lead to stabilisation of the various polymorphs at different temperature ranges, and may adjust properties, such as surface chemistry for catalysis, or the band gap for electronic applications. Roy and co-workers reported on the polymorphism in the Ga-Al-O system in the 1950s at the same time as their research with Ga\textsubscript{2}O\textsubscript{3} polymorphism.\textsuperscript{21} von Wartenberg and Reusch had previously shown in 1932 that solid solutions of \( \beta \)-Ga\textsubscript{2-x}Al\textsubscript{x}O\textsubscript{3} could be prepared at high temperatures, one of the earliest papers detailing polymorphism in the Ga-Al-O system.\textsuperscript{22} A hexagonal phase with composition GaAlO\textsubscript{3} was reported by Roy and co-workers, \textit{via} hydrothermal routes, although its structure was not assigned.\textsuperscript{21} This material was later investigated by MacDonald \textit{et al.}\textsuperscript{23} and several possible hexagonal space groups were suggested based on systematic absences in powder XRD patterns, and other new ternary phases also reported. More recent work by Inoue and co-workers on the Ga-Al-O system used solvothermal synthesis to prepare \( \gamma \)-Ga\textsubscript{2-x}Al\textsubscript{x}O\textsubscript{3} defect spinels.\textsuperscript{24-28} These mixed-metal \( \gamma \)-Ga\textsubscript{2-x}Al\textsubscript{x}O\textsubscript{3} spinels have been explored for some catalysis applications: including their use in the selective catalytic reduction (SCR) of NO by methane,\textsuperscript{25, 27-31} dehydrogenation of propane,\textsuperscript{32-33} dimethyl ether steam reforming.\textsuperscript{34} \( \gamma \)-Ga\textsubscript{2}O\textsubscript{3} supported on \( \gamma \)-Al\textsubscript{2}O\textsubscript{3} has been applied for photocatalysis.\textsuperscript{35}
Experimental

Solvothermal synthesis of mixed aluminium-gallium oxides was investigated using lower temperatures than applied previously by Inoue and co-workers\textsuperscript{24-28} using either 1,4-butadiol or isopropanol as solvent. Solvothermal synthesis of the solid solution Ga\textsubscript{5-x}Al\textsubscript{x}O\textsubscript{7}(OH) was achieved from 0.4 g (1.01 mmol) of Ga(acac)\textsubscript{3} (Sigma, 99.99%), where acac = acetylacetonate, and an appropriate amount of Al(acac)\textsubscript{3} (Merck, $\geq$98%), which were added to a 20 ml PTFE liner followed by the addition of 8 ml of 1,4-butadiol. The reaction mixture was stirred at room temperature for 10 minutes before being sealed inside a stainless-steel autoclave and placed inside a preheated fan assisted oven at 240 °C for 96 hours. After this time, the autoclave was allowed to cool naturally to ambient temperature and the vessel opened to reveal a white powder, which was dispersed by magnetic stirring in the mother liquor followed by addition of acetone to reduce the viscosity of the diol. The material was then collected by suction filtration, washed with further acetone, and dried overnight at 70 °C. To form $\gamma$-(Al\textsubscript{1-x}Ga\textsubscript{x})\textsubscript{2}O\textsubscript{3} 0.4 g (1.01 mmol) Ga(acac)\textsubscript{3} (Aldrich, 99.99%) and an appropriate amount of Al(O\textsubscript{i}Pr)\textsubscript{3} (Aldrich, $\geq$98%), to give a (2–x) : x molar ratio of Ga : Al ($0 \leq x \leq 1.8$), were added to a PTFE liner followed by the addition of 10 ml of 2-propanol. The reaction mixture was stirred at room temperature for 5 minutes before being sealed inside a stainless-steel autoclave and placed inside a preheated fan assisted oven at 240 °C for 24 hours. The autoclave was allowed to cool naturally to ambient temperature and the white solid product was collected by suction filtration and then washed with copious amounts of acetone before being dried at 70 °C overnight. Thermal decomposition of the solvothermally-prepared materials to $\beta$-(Al\textsubscript{1-x}Ga\textsubscript{x})\textsubscript{2}O\textsubscript{3} and $\alpha$-(Al\textsubscript{1-x}Ga\textsubscript{x})\textsubscript{2}O\textsubscript{3} was guided by thermoodffracctometry experiments (see below) and materials were then heated in air in muffle furnaces up to 1400 °C.

Powder XRD patterns were recorded at room temperature using a Panalytical X’Pert Pro MPD operating with monochromatic Cu K\textsubscript{α1} radiation and equipped with a PIXcel solid-state detector. Full pattern analysis of powder patterns was performed using the Pawley method within the TOPAS software to determine lattice parameters.\textsuperscript{36} A Bruker D8 Advance powder
diffractometer operating with Kα1/2 radiation and equipped with a VÅNTEC-1 solid-state detector with an Anton Parr XRK900 chemical reaction chamber was used to collect powder XRD with *in situ* heating. A typical data collection involved heating from 30 °C to 810 °C or 900 °C at 10 °C min⁻¹ with 30 °C intervals holding for 300 seconds at each interval prior to data collection to allow the temperature to equilibrate.

Scanning electron microscopy (SEM) images were recorded using a ZEISS GEMINI. A small amount of sample was placed on to a carbon tape prior to analysis. Transmission electron microscopy (TEM) was performed using a JEOL 2000FX instrument with samples placed on holey carbon copper grids *via* dispersion in acetone.

Thermogravimetric analysis (TGA) coupled with differential scanning calorimetry (DSC) was used to determine mass loss in samples upon heating from room temperature to usually 1000 °C using a Mettler Toledo TGA/DSC 1-600 instrument.

Solid-state ¹H NMR spectra were recorded using a Bruker Avance III spectrometer equipped with a 14.1 T wide-bore superconducting magnet (Larmor frequency of 600.13 MHz) and standard Bruker 1.3 mm magic angle spinning (MAS) probe (MAS rate of 55 kHz) at the University of St Andrews. ¹H MAS NMR spectra were recorded with signal averaging for 16 transients with a recycle interval of 60 s. Chemical shifts are reported in ppm relative to tetramethylsilane using L-alanine as a secondary solid reference (δCH₃ = 20.5 ppm).

Solid-state ²⁷Al NMR spectra were recorded using a Bruker Avance III spectrometer equipped with a 14.1 T wide-bore superconducting magnet (Larmor frequency of 156.4 MHz) and standard Bruker 3.2 mm MAS probe (MAS rate of 20 kHz) at the University of St Andrews. ²⁷Al MAS NMR spectra were recorded with signal averaging for between 1024 and 4096 transients with a recycle interval of 0.5 s for all materials apart except the β-Ga₂₋ₓAlₓO₃ series, for which a recycle interval of 3 s was used. An excitation pulse with inherent flip angle of ~4° was used to enable accurate quantitation. ¹H-²⁷Al cross polarisation (CP) MAS NMR spectra were recorded with a spin-lock pulse (ramped for ¹H) of 1 ms and high-power continuous wave decoupling of ¹H (ν₁ ≈ 80
kHz) was applied during acquisition. Signal averaging was carried out for between 10240 and 20480 transients with a recycle interval of 3 s. $^{27}$Al multiple-quantum (MQ) MAS NMR spectra were recorded using an amplitude-modulated z-filtered experiment. Signal averaging was carried out for between 240 and 1008 transients for each of up to 160 $t_1$ increments of 25 μs with a recycle interval of 0.5 s. Spectra are shown after shearing and referencing according to Pike et al. Chemical shifts are reported in ppm relative to 1.1 M Al(NO$_3$)$_3$ using Al(acac)$_3$ as a secondary solid reference ($\delta_{iso} = 0.0$ ppm).

Solid-state $^{71}$Ga NMR spectra were recorded using either a Bruker Avance II or Bruker Avance NEO console equipped with a 20.0 T wide-bore superconducting magnet (Larmor frequency of 259.3 MHz) and Bruker 1.3 mm double-broadband HXY probe (MAS rates of 50 to 55 kHz) or Jeol 1 mm double-resonance probe (MAS rate of 75 kHz) at the UK 850 MHz solid-state NMR facility. $^{71}$Ga MAS NMR spectra were recorded using a rotor-synchronised spin-echo pulse sequence with an echo delay of one rotor period (i.e., 13.3 to 20.0 μs). Signal averaging was carried out for between 3360 and 56000 transients with a recycle interval of between 0.5 and 2 s. Chemical shifts are reported in ppm relative to aqueous Ga(NO$_3$)$_3$ using either LaGaO$_3$ ($\delta_{iso} = 57$ ppm) or GaPO$_4$ berlinite ($\delta_{iso} = 111.2$ ppm) as secondary solid references.

The calculation of NMR parameters was carried out using the CASTEP density functional theory (DFT) code (version 18.1), employing the gauge-including projector augmented wave (GIPAW) approach to reconstruct the all-electron wavefunction in the presence of a magnetic field. Calculations were performed using the GGA PBE functional, with dispersion corrections provided by the scheme of Tkatchenko and Scheffler. Ultrasoft pseudopotentials were used with the inclusion of ZORA scalar relativistic effects. (A modified pseudopotential was used for gallium, see Supporting Information for more details.) A planewave energy cutoff of 60 Ry (~816 eV) was used, and integrals over the first Brillouin zone were performed using a Monkhorst-Pack grid with a $k$-point spacing of 0.03 or 0.04 2π Å$^{-1}$. Optimisation of atomic coordinates and unit cell parameters was carried out prior to the calculation of NMR parameters. Calculations were
performed on a computing cluster at the University of St Andrews, consisting of 90 32-core Intel Broadwell nodes, Infiniband FDR interconnect and a 300 TB GPFS distributed filesystem. Typical calculation times were between 3 and 10 h (geometry optimisation) and ~1 h (NMR parameters), using 48 cores. Isotropic shieldings, $\sigma_{\text{iso}}$, were obtained from the trace of the absolute shielding tensor, $\sigma$, and isotropic chemical shifts, $\delta_{\text{iso}}$, were given by $\delta_{\text{iso}} = - (\sigma_{\text{iso}} - \sigma_{\text{ref}}) / m$, where $\sigma_{\text{ref}}$ and $m$ had respective values of 562.4 ppm and 1.07 for $^{27}\text{Al}$ and 1740 ppm and 1.01 for $^{71}\text{Ga}$ (see Supporting Information). The quadrupolar coupling constant, $C_Q = eQV_{ZZ}/h$, and the asymmetry parameter, $\eta_Q = (V_{XX} - V_{YY})/V_{ZZ}$, are obtained directly from the principal components of the electric field gradient tensor, $V$. $Q$ is the nuclear quadrupole moment, for which values of 146.6 and 107 mb were used for $^{27}\text{Al}$ and $^{71}\text{Ga}$, respectively.

Results and Discussion

1. Ga$_{5-x}$Al$_x$O$_7$(OH) The hitherto unreported Ga$_{5-x}$Al$_x$O$_7$(OH) solid solution can be achieved for a composition range $0 \leq x \leq 1.5$ from solvothermal reaction between Ga(acac)$_3$ and Al(OiPr)$_3$ in 1,4-butanediol for 96 hours at 240 °C. The synthesis method is similar to that reported by Inoue and co-workers, who used solvothermal reactions to prepare $\gamma$-Ga$_2$$_{x}$Al$_x$O$_3$, but we have used lower temperatures and extended reactions times. The previous synthetic work was performed at 300 °C for just 2 hours in nitrogen atmosphere and the only products found in 1,4-butane diol were $\gamma$-Ga$_2$$_{x}$Al$_x$O$_3$ materials for $x \leq 1.5$. We found that shorter reaction times at 240 °C were unreliable as a synthesis route, yielding either $\gamma$-Ga$_2$O$_3$ with AlOOH, $\gamma$-Ga$_2$$_{x}$Al$_x$O$_3$ or GaOOH. We found that the same reaction can be performed in 1,5-pentanediol but the synthesis time must be even longer, requiring a minimum of 7 days, with shorter reaction times yielding only amorphous materials.

Figure 1 shows powder XRD profiles fitted using the Pawley refinement method against data from Ga$_{5-x}$Al$_x$O$_7$(OH) samples with $x = 0, 0.5, 1.0$ and 1.5. These fits were performed using space group $P6\overline{3}mc$, with initial lattice parameters from the published structure of Ga$_5$O$_7$(OH). Clear evidence for anisotropic peak broadening was found in all three samples, although this is less prominent with
increasing Al$^{3+}$ content, as there is an increase in the overall static disorder within the material, such that all reflections are further broadened. The use of Stephens’ phenomenological model of anisotropic peak broadening$^{46}$ was essential in order to obtain a satisfactory profile fit. Figure 2 shows the evolution of the lattice parameters with Ga : Al (see Table S1 for values of lattice parameters). The variation of the unit cell volume with elemental substitution follows Vegard’s law, with the volume of the material linearly decreasing with increasing aluminium substitution. Infrared spectroscopy shows an intense O-H stretching mode observed at 3300 cm$^{-1}$ (Figure S1), and a feature at 850 cm$^{-1}$ that is attributed to a (Ga,Al)-O-H bending mode, as a mode at a similar wavenumber was assigned to this in both Ga$_5$O$_{7}$O(OH)$^{15}$ and in a computational study on Al$_5$O$_{7}$(OH)$^{47}$ Solid-state $^1$H NMR spectra of the Ga$_{5-x}$Al$_x$O$_{7}$(OH) materials (Figure S2) also confirm the presence of (Ga,Al)-OH species, with chemical shifts between 7.7-8.0 ppm.
**Figure 1:** Pawley refinements against powder XRD data ($\lambda = 1.54059$ Å) for Ga$_{5-x}$Al$_x$O$_7$(OH), ($0 \leq x \leq 1.5$), with insets showing the fit to a region of the data when the Stephens’ parameters were not used to correct for anisotropic peak broadening.
Figure 2: Plot of (a) hexagonal lattice parameters and (b) unit cell volume vs composition for Ga$_{5-x}$Al$_x$O$_7$(OH). The values for the end members (black squares) are taken from the literature for $x = 0$ and $x = 5$. The values for $x = 0.5, 1$ and $1.5$ (open squares) were determined in this work, while the values for $x = 2.5$ (black circles) are those reported for ‘hexagonal GaAlO$_3$’ by Macdonald et al. The linear fits (grey lines) are the result of linear regression analysis against all of the data points.

MacDonald et al. reported a phase they identified as GaAlO$_3$ in 1967 and their refined lattice parameters ($a = 5.70$ Å, $c = 8.92$ Å, $V = 251.0$ Å$^3$) fit very well with the trend in unit cell volume seen in Figure 2. It seems likely the oxyhydroxides that we now report are related materials, with the earlier assignment of composition incorrect (note that the previous work used high-temperature
hydrothermal synthesis, which may have given access to materials with a greater Al content than we have achieved). Ga$_3$O$_7$(OH) and Al$_3$O$_7$(OH) are forms of the mineral 5Al$_2$O$_3$.H$_2$O, known as akdalaite, with a synthetic form of the material initially described as tohdite. It is interesting to note that there are no reported non-aqueous solvothermal syntheses of Al$_3$O$_7$(OH), and it is usually synthesised by treating aluminium salts, or aluminium oxides, hydrothermally at temperatures in excess of 240 °C, typically with the application of external pressure. We found that Al$_3$O$_7$(OH) could not be prepared by reaction of either Al(O'Pr)$_3$ or Al(acac)$_3$ in 1,4-butanediol at 240 °C, despite a wide range of reaction times being investigated.

TGA of Ga$_{3.5}$Al$_{1.5}$O$_7$(OH) shows that a gradual mass loss of 1.5% commences immediately upon heating to ~400 °C, followed by a larger mass loss of 2.5% occurring between 400 – 600 °C (Figure S3). This second mass loss is consistent with the dehydration of Ga$_{3.5}$Al$_{1.5}$O$_7$(OH) since it occurs over the same temperature range that the material is observed to decompose in the thermodiffractometry experiment (see below) and the mass loss of 2.5% is consistent with the expected mass loss of ~2.2% on conversion to “Ga$_{1.4}$Al$_{0.6}$O$_3$”. The first observed gradual mass loss could possibly be attributed to loss of excess surface diol. TEM shows that Ga$_{3.5}$Al$_{1.5}$O$_7$(OH) consists of large, thin hexagonal plates (Figure 3). The anisotropic peak broadening observed by XRD is likely a consequence of morphology of the material, as was also reported for the pure gallium analogue.

Figure 3 (a) SEM image and (b) TEM image of Ga$_{3.5}$Al$_{1.5}$O$_7$(OH).
The structure of Ga$_5$O$_7$(OH) contains both tetrahedral and octahedral sites for the trivalent cations, occupied in a 1 : 4 ratio, respectively. Given the different coordination preferences of Al and Ga, solid-state NMR spectroscopy was used to determine the relative proportion of each site occupied in the samples of Ga$_{5-x}$Al$_x$O$_7$(OH) with $x = 0, 0.5, 1$ and 1.5.

In oxides, the $^{27}$Al isotropic chemical shift ranges for tetrahedral and octahedral coordination environments are well separated at 80 to 50 and 15 to –10 ppm, respectively. In principle, the same is true for $^{71}$Ga NMR, which has isotropic chemical shift ranges of ca. 220 to 110 and ca. 80 to –40 ppm, respectively for tetrahedrally and octahedrally coordinated Ga, respectively, but the larger second-order quadrupolar broadening usually requires the use of higher external magnetic fields (here, $B_0 = 20.0$ T) to afford sufficiently high resolution to allow accurate quantitation of these species. Figure 4(a) shows the $^{71}$Ga MAS NMR spectrum of Ga$_5$O$_7$(OH), which contains three resonances with NMR parameters shown in Table 1 (indicated by the red and grey lines on Figure 4(a)). These resonances can be assigned by their isotropic chemical shifts and relative intensities to octahedral Ga1 ($\delta_{iso} = 80$ ppm), octahedral Ga2 ($\delta_{iso} = 20$ ppm) and tetrahedral Ga3 ($\delta_{iso} = 132$ ppm) in the structure of Ga$_5$O$_7$(OH) reported by Playford et al. The relatively small quadrupolar coupling constant ($C_Q$) observed for Ga2 indicates that its coordination environment is close to ideal, whereas the much larger $C_Q$ observed for Ga1 reflects the fact that this site is coordinated by five oxides and one hydroxide, leading to a lowering of the local symmetry, a distortion of the coordination environment, and a much larger electric field gradient (EFG, responsible for the magnitude of $C_Q$) at the Ga site. Interestingly, the signal attributed to tetrahedral Ga3 also displays a very large $C_Q$ compared to the β polymorph of Ga$_2$O$_3$ (ca. 11 MHz for the tetrahedral site). However, it can be seen from the structure of Playford et al. that this site in Ga$_5$O$_7$(OH) is significantly distorted, with O-Ga-O angles ranging from 102 to 115°.
**Figure 4** (a) $^{71}$Ga (20.0 T, 75 kHz MAS) NMR spectrum of Ga$_5$O$_7$(OH) (black), spectrum simulated using the parameters given in Table 1 (red) and individual lineshapes corresponding to the three Ga signals (grey). (b) $^{71}$Ga (20.0 T, 55 kHz MAS) NMR spectra, (c) $^{27}$Al (14.1 T, 20 kHz MAS) NMR spectra and (d) $\delta_1$ projections of $^{27}$Al (14.1 T, 20 kHz MAS) MQMAS NMR spectra (see Figure S4 for two-dimensional spectra) of Ga$_{5-x}$Al$_x$O$_7$(OH) ($x = 0.5, 1.0, 1.5$).

**Table 1.** $^{71}$Ga NMR parameters of Ga$_5$O$_7$(OH) obtained from fitting the spectrum in Figure 4(a).

| Site | Relative integral | $\delta_{iso}$ (ppm) | $C_Q$ / MHz | $\eta_Q$ |
|------|------------------|----------------------|-------------|---------|
| Ga1  | 3.0              | 81(2)                | 11.3(2)     | 0.75(5) |
| Ga2  | 1.0              | 20(2)                | 5.7(2)      | 0.05(5) |
| Ga3  | 1.0              | 132(5)               | 15.0(2)     | 0.05(2) |
Figures 4(b) and 4(c) show $^{71}$Ga and $^{27}$Al MAS NMR spectra of Ga$_{5-x}$Al$_x$O$_7$(OH) with $x = 0.5, 1.0$ and 1.5. It is particularly apparent from the $^{27}$Al NMR spectra that the Al shows a strong preference for substitution into the octahedral sites, with an Al$^{IV}$ : Al$^{VI}$ ratio of ~1 : 220 observed for Ga$_{3.5}$Al$_{1.5}$O$_7$(OH) (cf. 1 : 4 for random substitution). Interpreting the $^{71}$Ga NMR spectra is more challenging as the resonances are not as well resolved as for $^{27}$Al, and the signal from tetrahedral Ga3 is so broad that it is difficult to detect visually that its relative proportion is increasing. Accurate spectral decomposition also becomes more challenging as the local disorder introduced by Al leads to further broadening of the spectral resonances. High-resolution $^{27}$Al multiple-quantum (MQ) MAS NMR spectra were recorded for these materials and the isotropic ($\delta_1$) projections are shown in Figure 4(d) (see Figure S4 for the two-dimensional spectra). Surprisingly, the MQMAS spectra reveal three signals for octahedral Al for all three compositions. While it is not possible to extract $\delta_{\text{iso}}$ and $C_Q$ directly from the MQMAS spectrum of a disordered material (owing to the distribution of these two parameters arising from the inherent distribution of chemical sites present), the position of the centre of gravity of a resonance within the spectrum can still provide information on the mean chemical shift, $\langle \delta_{\text{iso}} \rangle$, and mean quadrupolar product, $\langle P_Q \rangle$, where

$$P_Q = C_Q \left[ 1 + \left( \frac{n_Q}{3} \right)^2 \right]^{1/2}.$$  

Table 2 reports these mean values for the three resonances observed for each of the three samples of Ga$_{5-x}$Al$_x$O$_7$(OH). The first, signal I, has values of $\langle \delta_{\text{iso}} \rangle$ and $\langle P_Q \rangle$ similar to those predicted for substitution of Al onto site 1, and signal III values similar to those predicted for substitution onto site 2. Signal II, however, has a $\langle \delta_{\text{iso}} \rangle$ value consistent with substitution onto site 1, but different $\langle P_Q \rangle$, suggesting some variation in the local or medium-range environment.
Table 2. $^{27}$Al NMR parameters of Ga$_{5-x}$Al$_x$O$_7$(OH) obtained from the MQMAS spectra shown in Figure S4 (and the corresponding projections shown in Figure 4(d)).

|            | Ga$_{4.5}$Al$_{0.5}$O$_7$OH | Ga$_{4.0}$Al$_{1.0}$O$_7$OH | Ga$_{3.5}$Al$_{1.5}$O$_7$OH |
|------------|----------------------------|----------------------------|-----------------------------|
| $\langle \delta_{iso} \rangle$ (ppm) | $\langle \delta_{iso} \rangle$ (ppm) | $\langle \delta_{iso} \rangle$ (ppm) | $\langle \delta_{iso} \rangle$ (ppm) |
| Signal I   | 21(1)                      | 21(1)                      | 20(1)                       |
|            | 4.6(2)                     | 4.7(2)                     | 5.1(2)                      |
| Signal II  | 20(1)                      | 19(1)                      | 18(1)                       |
|            | 3.5(2)                     | 3.8(2)                     | 3.8(2)                      |
| Signal III | 11(1)                      | 11(1)                      | 11(1)                       |
|            | 2.2(2)                     | 2.1(2)                     | 2.1(2)                      |

DFT calculations can often be used to provide insight into the NMR spectra of disordered materials where the disorder arises from simple substitutions of one atom for another, as is expected to be the case for Ga$_{5-x}$Al$_x$O$_7$OH. In this case, seven model structures were generated by substituting one or two Al atoms into the structure of Ga$_5$O$_7$OH of Playford et al., corresponding to 10% and 20% Al substitution, respectively. For further details of the model structures, see Section S2 of the Supporting Information. All models were optimised prior to calculation of the reported energies and NMR parameters. When considering the model structures with one Al per unit cell, substitution onto site 1 (i.e., Ga1) is most energetically favoured (by 0.215 eV per cell (10.4 kJ mol$^{-1}$) relative to Ga2 and 0.519 eV per cell (25.0 kJ mol$^{-1}$) relative to Ga3). Given the greater energetic preference for substitution for Ga1, as well as the greater population number of these sites in the crystal structure, it is unsurprising that a significant amount of Al1 is observed in experimental NMR spectra and that Al3 is not observed at all. However, experimentally an additional resonance is observed in the $^{27}$Al MQMAS spectrum, even for the sample with the lowest Al content, perhaps suggesting that the Al atoms adopt some degree of ordering or clustering.

By including two Al atoms per cell, it is possible to investigate the effects of their relative positions on the calculated $^{27}$Al NMR parameters. Again, it is seen that placing the second Al also on site 1 is most energetically favourable (0.276 eV per cell relative to Al1+Al2 and 0.556 eV per cell relative
to Al\textsubscript{1}+Al\textsubscript{3} and that the two possible relative positions of Al\textsubscript{1}+Al\textsubscript{1} (\textit{i.e.}, bridged by Al-OH-Al or isolated) are energetically very similar (with a difference of only 0.060 eV per cell). However, the values of $C_Q$ calculated for these two atomic arrangements is quite different, with the Al in an Al\textsubscript{1}-OH-Al\textsubscript{1} motif having a $C_Q$ of 5.0 MHz and two isolated Al\textsubscript{1} having a $C_Q$ of 3.4 MHz (compared to 4.7 MHz for a single isolated Al\textsubscript{1} in the cell). This suggests that signals I and II in Table 2 can be assigned to Al\textsubscript{1}-OH-Al\textsubscript{1} and isolated Al\textsubscript{1}, respectively. The presence of Al\textsubscript{2} in the same cell as Al\textsubscript{1} is predicted to lead to an even smaller $C_Q$ for Al\textsubscript{1} of 2.8 MHz and, while a clear resonance is not observed for this species (owing to the low Al population on site 2), such species may be responsible for the tail to lower $\delta_1$ seen in Figure 4(d). The $^{27}$Al NMR spectra, therefore, can be seen as evidence that, not only does Al have a strong preference for site 1, but that the Al cannot be homogeneously distributed throughout the material as, even for the lowest Al content (Ga\textsubscript{4.5}Al\textsubscript{0.5}O\textsubscript{7}OH), a signal is observed for Al\textsubscript{1} near to other Al\textsubscript{1} (\textit{i.e.}, Al-rich regions).

It should also be noted in the $^{71}$Ga MAS NMR spectra of Ga\textsubscript{5-}$\times$Al\textsubscript{5}O\textsubscript{5}OH, shown in Figure 4(b), that an additional resonance at $\sim$145 ppm is observed. There is no evidence from any of the calculations that Al substitution should give rise to a resonance in this position and the most likely assignment is that it is part of the lineshape for the tetrahedral Ga in a minor impurity of $\beta$-Ga\textsubscript{2-}$\times$Al\textsubscript{5}O\textsubscript{3} (see below for further discussion of this phase).

2. $\gamma$-Ga\textsubscript{2-}$\times$Al\textsubscript{5}O\textsubscript{3} The synthesis of $\gamma$-Ga\textsubscript{2-}$\times$Al\textsubscript{5}O\textsubscript{3} in 1,4-butanediol at 240 °C was found to be rather unreliable at short reaction times, often forming unwanted by-products, such as AlOOH (boemite) and diaspor-type GaOOH (tsunagallite). However, changing the solvent to isopropanol was found to provide a reliable route to $\gamma$-Ga\textsubscript{2-}$\times$Al\textsubscript{5}O\textsubscript{3} spinels and solid solutions containing up to 90% Al$^{3+}$ could be obtained (\textit{i.e.}, $x \leq 1.8$). This exceeds the compositional range reported by Inoue and co-workers in their higher temperature synthesis in 1,4-butanediol.\textsuperscript{24} The use of isopropanol may allow better mixing of the regents due to its lower viscosity. The XRD profiles, Figure 5, show that these materials have very broad Bragg reflections indicative of poorly crystalline materials, and
likely consist of nano-sized crystallites. Scherrer analysis of the peak broadening gives estimated crystallite domain size ranging from ~10 nm (x = 0) down to ~ 7 nm (x = 1.8), confirming the nanocrystalline nature of the materials. BET surface area measurements confirmed that all of these materials have a very high surface area ~200 m²g⁻¹. The powder XRD profiles can be fitted to a cubic crystal system with space group $Fd\overline{3}m$, typical for spinel oxides, and Pawley refinements allowed the unit cell lattice parameter to be refined, revealing a linear decrease in this with the increase in Al³⁺ content (Figure 6). An peak due to an unidentified impurity around 42.5° 2θ is prominent in the 90% Al³⁺ substituted spinel indicating that 90% has likely reached the limit of substitution in this solid solution by this synthesis method. No Rietveld analysis was undertaken owing to the broadness of the peaks. EDX using the SEM gives good agreement with the expected metal ratios in the samples (see Table S6).
Figure 5 Pawley refinements against powder XRD data ($\lambda = 1.54059$ Å) for $\gamma$-Ga$_{2-x}$Al$_x$O$_3$ spinels ($0 \leq x \leq 1.8$). * denotes an impurity phase in the $x = 1.8$ material.
Figure 6 Plot of spinel lattice parameter for $\gamma$-$\text{Ga}_{2-x}\text{Al}_x\text{O}_3$ with increasing aluminium substitution, and comparison to that of a reference $\gamma$-$\text{Al}_2\text{O}_3$ material.$^{55}$

The $^{71}\text{Ga}$ and $^{27}\text{Al}$ MAS NMR spectra of $\gamma$-$\text{Ga}_{2-x}\text{Al}_x\text{O}_3$ are shown in Figure 7. All spectra contain broadened resonances with characteristic tails to lower shift, indicative of static disorder. For $^{71}\text{Ga}$, it should be noted that the signal-to-noise ratio is lower for samples with greater Al content owing to a combination of the low Ga content and the very small volume (~0.8 μL) of the 1 mm rotors required to achieve the rapid MAS rate. As for the $\text{Ga}_5-x\text{Al}_x\text{O}_7$(OH) series above, the Al in $\gamma$-$\text{Ga}_{2-x}\text{Al}_x\text{O}_3$ exhibits a strong preference for octahedral coordination and even with 90% Al substitution ($x = 1.8$), 95% of the octahedral cations are Al, but only 74% of the tetrahedral cations. This is consistent with earlier work by Areán et al.$^{56}$ who used $^{27}\text{Al}$ and $^{71}\text{Ga}$ MAS NMR spectroscopy to characterise $\gamma$-$\text{Ga}_{2-x}\text{Al}_x\text{O}_3$ with $x = 0.4$, 1.0 and 1.6 and observed very similar behaviour. From the integrated spectral intensities of the $^{71}\text{Ga}$ and $^{27}\text{Al}$ MAS NMR spectra, it is possible to derive the bulk compositions for the $\gamma$-$\text{Ga}_{2-x}\text{Al}_x\text{O}_3$ materials, shown in Table 3.
Figure 7 (a) $^{71}$Ga (20.0 T, 75 kHz MAS) NMR spectra and (b) $^{27}$Al (14.1 T, 20 kHz MAS) NMR spectra of $\gamma$-Ga$_{2-x}$Al$_x$O$_3$.

Table 3. Relative occupation of tetrahedral and octahedral sites in $\gamma$-Ga$_{2-x}$Al$_x$O$_3$ as determined from the $^{27}$Al and $^{71}$Ga MAS NMR spectra in Figure 7, and the overall formula (represented in defect spinel and AB$_2$O$_4$ notation) derived from these.

| $x$ | $^{27}$Al NMR | $^{71}$Ga NMR | Formula |
|-----|---------------|---------------|---------|
|     | % $\text{Al}^{\text{IV}}$ | % $\text{Al}^{\text{VI}}$ | % $\text{Ga}^{\text{IV}}$ | % $\text{Ga}^{\text{VI}}$ | defect spinel | AB$_2$O$_4$ |
| 0.0 | — | — | 26.8 | 73.2 | $\gamma^-(\text{Ga}_{0.035}\text{Al}_{0.365})_{\text{tet}}[\text{Ga}_{1.465}]_{\text{oct}}\text{O}_3$ | (Ga$_{0.713}$)$_{\text{tet}}[\text{Ga}_{1.953}]_{\text{oct}}\text{O}_4$ |
| 0.6 | 5.2 | 94.8 | 33.6 | 66.4 | $\gamma^-(\text{Ga}_{0.470}\text{Al}_{0.031})_{\text{tet}}[\text{Ga}_{0.930}\text{Al}_{0.069}]_{\text{oct}}\text{O}_3$ | (Ga$_{0.626}$)$_{\text{tet}}[\text{Ga}_{1.309}\text{Al}_{0.701}]_{\text{oct}}\text{O}_4$ |
| 1.0 | 7.7 | 92.3 | 39.3 | 60.7 | $\gamma^-(\text{Ga}_{0.393}\text{Al}_{0.077})_{\text{tet}}[\text{Ga}_{0.607}\text{Al}_{0.023}]_{\text{oct}}\text{O}_3$ | (Ga$_{0.524}$)$_{\text{tet}}[\text{Ga}_{0.476}\text{Al}_{0.524}]_{\text{oct}}\text{O}_4$ |
| 1.5 | 14.7 | 85.3 | 63.5 | 36.5 | $\gamma^-(\text{Ga}_{0.318}\text{Al}_{0.221})_{\text{tet}}[\text{Ga}_{0.183}\text{Al}_{1.282}]_{\text{oct}}\text{O}_3$ | (Ga$_{0.424}$)$_{\text{tet}}[\text{Ga}_{0.576}\text{Al}_{1.704}]_{\text{oct}}\text{O}_4$ |
| 1.8 | 19.4 | 80.6 | 61.8 | 38.2 | $\gamma^-(\text{Ga}_{0.124}\text{Al}_{0.936})_{\text{tet}}[\text{Ga}_{0.076}\text{Al}_{1.345}]_{\text{oct}}\text{O}_3$ | (Ga$_{0.165}$)$_{\text{tet}}[\text{Ga}_{0.165}\text{Al}_{1.935}]_{\text{oct}}\text{O}_4$ |

In all five materials, the octahedral sites are almost fully occupied, meaning that the vacancies are located mainly on the tetrahedral sites. In the pure gallium oxide sample the tetrahedral : octahedral ratio is $\sim 1 : 2.7$, which is a substantially larger occupancy of the octahedral sites than found in disordered gamma gallium oxide prepared from amorphous gels (ratio of $1 : 2.1$). These NMR and
compositional data are also plotted graphically in Figure 8 to show how the changes in relative octahedral : tetrahedral proportion and site occupancy depends upon the composition of the spinel. It should be noted that this is an oversimplification, however, since partial occupation of non-spinel sites may also be possible, as has been found in both the crystalline pure $\gamma$-Al$_2$O$_3$ and $\gamma$-Ga$_2$O$_3$ structures.$^{15-16, 20}$ These extra sites also have tetrahedral and octahedral coordination, but the disordered nature of these materials causes broadening in the NMR spectra and it was not possible to resolve additional signals for these sites. It has also been proposed that the occupancy of extra sites is greater in the poorly crystalline samples of $\gamma$-Ga$_2$O$_3^{16}$ compared to more crystalline samples, and so it is likely that similar additional sites are occupied in these new materials. Additionally, it is known that $\gamma$-Ga$_2$O$_3$ exhibits a surface reconstruction that is enriched in octahedral sites$^{16}$ and $^1$H-$^{27}$Al cross-polarisation (CP) MAS NMR experiments (Figure S10) support a similar reconstruction here. The CP MAS experiment transfers magnetisation from $^1$H (which should be found mainly in surface OH species) to nearby $^{27}$Al nuclei and is, therefore, effectively surface selective. However, it should be noted that, even in these surface-selective spectra, very little signal is observed for pentacoordinate Al, which has previously been observed by NMR spectroscopy for $\gamma$-Al$_2$O$_3$ using surface-selective dynamic nuclear polarisation (DNP) measurements,$^{57-59}$ and has additionally been observed in MAS experiments by Areán et al. for $\gamma$-Ga$_{2-x}$Al$_x$O$_3$ with $x = 0.4, 1.0$ and $1.6$. It can, therefore, be concluded that the materials studied here have a surface that is enriched in octahedral Al relative to the bulk material.
Figure 8 (a) Plot showing the proportion of tetrahedral (IV) and octahedral (VI) Al and Ga cations (solid lines and symbols), and the overall proportion of octahedral and tetrahedral cations (dashed lines), in \( \gamma \)-Ga\(_{2-x}\)Al\(_x\)O\(_3\). (b) Plot showing the amount of Al substitution on the tetrahedral and octahedral sites (solid lines) and the overall level of Al substitution in the \( \gamma \)-Ga\(_{2-x}\)Al\(_x\)O\(_3\) (dashed line). All values were derived from the integrated spectral intensities from the \(^{27}\)Al and \(^{71}\)Ga NMR spectra shown in Figure 7.

3. \( \beta \)-Ga\(_{2-x}\)Al\(_x\)O\(_3\) and \( \alpha \)-Ga\(_{2-x}\)Al\(_x\)O\(_3\) The thermal decomposition of the Ga\(_{5-x}\)Al\(_x\)O\(_7\)(OH) materials is complex and, as for the pure aluminium\(^{60}\) and gallium\(^{15}\) end members, occurs via mixtures of poorly crystalline \( \varepsilon \)-(Al,Ga)\(_2\)O\(_3\) and \( \kappa \)-(Al,Ga)\(_2\)O\(_3\), where it is difficult to determine if phase separation has taken place (Figures S4 and S5). Instead, we focus on the high-temperature phase transformation of the \( \gamma \)-Ga\(_{2-x}\)Al\(_x\)O\(_3\) spinels, since this occurs without phase separation. Substitution of aluminium for gallium in the spinel enhances the thermal stability of these phases over the pure
gallium version (Figure S11): while pure nano-crystalline $\gamma$-Ga$_2$O$_3$ transforms directly into the thermodynamically stable polymorph, $\beta$-Ga$_2$O$_3$, at around 750 °C, whilst a higher temperature (> 900 °C) is required for the transformation of aluminium-substituted samples. At 90% Al substitution, the spinel converts directly into $\alpha$-Ga$_{0.2}$Al$_{1.8}$O$_3$ without prior transformation into the $\beta$ polymorph. Rietveld analysis of a sample of $\alpha$-Ga$_{0.2}$Al$_{1.8}$O$_3$ shows that the occupancy of the metal site for Ga and Al refines to 0.09 and 0.91, respectively, in agreement with the nominal formula (Figure 9 and Table 4). $^{27}$Al and $^{71}$Ga MAS NMR spectra are consistent with the presence of only octahedral cations in this material (Figure S13).

![Rietveld plot of $\alpha$-Ga$_{0.2}$Al$_{1.8}$O$_3$ against powder X-ray diffraction data ($\lambda = 1.54059$ Å).](image)

**Figure 9** Rietveld plot of $\alpha$-Ga$_{0.2}$Al$_{1.8}$O$_3$ against powder X-ray diffraction data ($\lambda = 1.54059$ Å).

**Table 4** Refined crystal parameters for $\alpha$-Ga$_{0.2}$Al$_{1.8}$O$_3$. Lattice parameters $a = 4.78281(5)$ Å, $c = 13.04096(15)$ Å, space group $R\bar{3}cH$. $R_p = 12.5\%$, $wR_p = 19.0\%$, $GOF = 1.247$. The thermal parameter for oxygen was fixed to achieve a satisfactory fit.

| Atom | Wyckoff site | x  | y  | $z$  | Occupancy | $B_{eq}$ / Å$^2$ |
|------|--------------|----|----|------|------------|----------------|
| Ga   | 12c          | 0  | 0  | 0.35289(8) | 0.09(6)     | 0.22(5)        |
| Al   | 12c          | 0  | 0  | 0.35289(8) | 0.91(6)     | 0.22(5)        |
| O    | 18e          | 0.3057(3) | 0  | 0.25 | 1.0        | 0.22           |
Transformation of the mixed aluminium-gallium oxide spinels into phase-pure $\beta$-Ga$_{2-x}$Al$_x$O$_3$ occurs for up to 65% Al$^{3+}$ substitution ($x = 1.3$), while the spinel phase separates into $\beta$-Ga$_{2-x}$Al$_x$O$_3$ and $\alpha$-Ga$_{2-x}$Al$_x$O$_3$ for $1.3 < x < 1.8$. Rietveld refinement against powder XRD data showed that no other crystalline phases were present in the $\beta$-Ga$_{2-x}$Al$_x$O$_3$ samples (Figure 10). Two constraints were placed during the refinement: (i) the total occupancy of each site was fixed at 1.0 to maintain the charge balance against the oxide and (ii) the total intended Al:Ga ratio from the synthesis was fixed. Refinement statistics and refined crystal parameters for all samples can be found in the Supporting Information Tables S7-S10. The change in the cell volume upon increasing aluminium content follows a linear relationship, obeying Vegard’s law and a decrease in the cell parameters with increasing aluminium content is expected owing to the smaller size of the Al$^{3+}$ cation, whilst an increase in the $\beta$ cell angle is also seen.
The structure refinements show that for all samples there is a significant amount of aluminium on the tetrahedral site, even for that with the smallest aluminium content. The $\text{Al}^{(IV)} : \text{Al}^{(VI)}$ ratio in the $\beta$ polymorph remains close to 1 : 2 across the composition range, but shows a small increase (i.e., an increase in tetrahedral occupation) with increasing Al substitution over the values of $x$ between 0.2 and 1.3. While Al still displays a preference for octahedral coordination (the $\text{Al}^{(IV)} : \text{Al}^{(VI)}$ ratio in $\beta$-$\text{Ga}_{2-x}\text{Al}_x\text{O}_3$ is 1 : 1), this preference is less pronounced than observed above for $\text{Ga}_5-x\text{Al}_x\text{O}_7(\text{OH})$ and $\gamma$-$\text{Ga}_{2-x}\text{Al}_x\text{O}_3$. This conclusion is also supported by DFT calculations, which
suggest that substitution of Al onto a tetrahedral site in $\beta$-Ga$_{2-x}$Al$_x$O$_3$ is less disfavoured than in Ga$_{5-x}$Al$_x$O$_7$OH, with an energy penalty of ~2.0 kJ per mole of cations in $\beta$-Ga$_{1.75}$Al$_{0.25}$O$_3$, compared with ~5.2 kJ per mole of cations for Ga$_{4.5}$Al$_{0.5}$O$_5$OH (see Supporting Information for details). $^{27}$Al MAS NMR spectroscopy (Figure 11) confirms that Al adopts tetrahedral and octahedral coordination throughout the series, with Al$^{(IV)}$ : Al$^{(VI)}$ varying systematically from 1 : 2.25 (~31% tetrahedral Al) for $x = 0.2$ to 1 : 1.44 (~41% tetrahedral Al) for $x = 1.3$.

**Figure 11** $^{27}$Al (14.1 T, 20 kHz MAS) NMR spectra of $\beta$-Ga$_{2-x}$Al$_x$O$_3$. The minor resonance at ~50 ppm in all spectra is a spinning sideband.

As shown in Figure 12(a), the relative site occupancies derived from the Rietveld refinements and $^{27}$Al NMR spectra are in good agreement for all compositions. Figure 12(b) shows the fraction of octahedral and tetrahedral sites occupied by Al (from the average of the values obtained from the Rietveld refinements and $^{27}$Al NMR spectra) for each composition, which confirms the slight preference for Al to occupy octahedral sites across the whole composition range. The average overall formulae derived from these data for all $\beta$-Ga$_{2-x}$Al$_x$O$_3$ materials studied are given in Table 5.
Figure 12 (a) Plot showing the proportion of tetrahedral (IV) and octahedral (VI) Al sites in $\beta$-Ga$_2$-$x$Al$_x$O$_3$, as determined by Rietveld refinement (solid lines) and $^{27}$Al NMR spectroscopy (dashed lines). (b) Plot showing the proportion of Al substitution on the tetrahedral and octahedral sites (solid lines) and the overall level of Al substitution in the $\beta$-Ga$_2$-$x$Al$_x$O$_3$ (dashed line). Note that the error bars in (a) are mainly smaller than the size of the points.
Table 5. Relative occupation of tetrahedral and octahedral sites in $\beta$-Ga$_{2-x}$Al$_x$O$_3$ as determined from the average of the values from Rietveld refinement and $^{27}$Al MAS NMR spectra, and the overall formula derived from these.

| x    | Al$^{IV}$ (%) | Al$^{VI}$ (%) | Formula                                      |
|------|---------------|---------------|----------------------------------------------|
| 0.0  | —             | —             | $\beta$-(Ga$_{1.0}$)$_{tet}$[Ga$_{1.0}$]$_{oct}$O$_3$ |
| 0.2  | 32.8          | 67.2          | $\beta$-(Ga$_{0.934}$Al$_{0.066}$)$_{tet}$[Ga$_{0.866}$Al$_{0.134}$]$_{oct}$O$_3$ |
| 0.4  | 34.3          | 65.7          | $\beta$-(Ga$_{0.863}$Al$_{0.137}$)$_{tet}$[Ga$_{0.737}$Al$_{0.263}$]$_{oct}$O$_3$ |
| 0.6  | 334.6         | 65.4          | $\beta$-(Ga$_{0.792}$Al$_{0.208}$)$_{tet}$[Ga$_{0.608}$Al$_{0.392}$]$_{oct}$O$_3$ |
| 0.8  | 36.6          | 63.4          | $\beta$-(Ga$_{0.708}$Al$_{0.292}$)$_{tet}$[Ga$_{0.492}$Al$_{0.508}$]$_{oct}$O$_3$ |
| 1.0  | 37.6          | 62.4          | $\beta$-(Ga$_{0.624}$Al$_{0.376}$)$_{tet}$[Ga$_{0.376}$Al$_{0.624}$]$_{oct}$O$_3$ |
| 1.2  | 40.9          | 59.1          | $\beta$-(Ga$_{0.509}$Al$_{0.491}$)$_{tet}$[Ga$_{0.291}$Al$_{0.709}$]$_{oct}$O$_3$ |
| 1.3  | 41.0          | 59.0          | $\beta$-(Ga$_{0.466}$Al$_{0.534}$)$_{tet}$[Ga$_{0.234}$Al$_{0.766}$]$_{oct}$O$_3$ |

There is very little difference in the refined crystal structure parameters between samples fired at 1200 °C and 1400 °C (Table S11), implying that the Al adopts tetrahedral coordination immediately upon phase transformation from the mixed-metal spinels, rather than forming an initial $\beta$ polymorph with a smaller number of tetrahedral Al species, followed by rearrangement at a higher temperature.

As would be expected, the average Al/Ga-O interatomic distance becomes smaller with increasing aluminium substitution in $\beta$-Ga$_{2-x}$Al$_x$O$_3$ with an average Al/Ga-O tetrahedral distance decrease from 1.816 Å to 1.789 Å and an average Al/Ga-O octahedral distance from 2.005 Å to 1.944 Å from x = 0.2 to x = 1.3, respectively (see Table S12). Pure $\beta$-Ga$_2$O$_3$ shows a significant distortion of the octahedral sites away from regular octahedral geometry, which is also present in all $\beta$-Ga$_{2-x}$Al$_x$O$_3$ samples in this work. The tetrahedral sites also appear significantly distorted for all samples, with the O-Ga/Al-O angles falling in the range of 104 – 120°, a feature also observed in the single-crystal re-investigation of $\beta$-Ga$_2$O$_3$ by Åhman et al. The $^{27}$Al NMR spectra of $\beta$-Ga$_{2-x}$Al$_x$O$_3$
Figure 11 confirm that there is a large EFG at the tetrahedral site, leading to $C_Q$ values of $\sim 5.0$ MHz (and a similarly large $C_Q$ of $\sim 11$ MHz is observed for $\beta$-Ga$_2$O$_3$).

Conclusions

Solvothermal synthesis allows the formation of mixed aluminium-gallium oxides and hydroxides using lower temperatures than previously reported. The new solid solution $\text{Ga}_{5-x}\text{Al}_x\text{O}_7(\text{OH})$ ($0.5 \leq x \leq 1.5$) has been structurally authenticated and the ‘hexagonal GaAlO$_3$’ reported in the earlier literature is a likely member of this family. The $\gamma$-$\text{Ga}_{2-x}\text{Al}_x\text{O}_3$ spinels form as poorly crystalline powders that can be thermally transformed into the high-temperature phases $\beta$-$\text{Ga}_{2-x}\text{Al}_x\text{O}_3$ ($0 \leq x \leq 1.3$) and $\alpha$-$\text{Ga}_{2-x}\text{Al}_x\text{O}_3$ ($x = 1.8$). This provides highly crystalline samples for which a detailed solid-state NMR spectroscopic investigation allows the distribution of site occupancies to be determined. Given the growing interest in gallium oxide polymorphs in applications such as electronics and photocatalysis, and the longstanding study of aluminium oxides as catalysts supports in heterogeneous catalysis, our results will provide reference data for understanding structure-property relationships in these fields.

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