Optical and dielectric properties of NaCoPO$_4$ in the three phases $\alpha$, $\beta$ and $\gamma$

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In this work, we are interested in the synthesis of monophosphate $\alpha$-NaCoPO$_4$, $\beta$-NaCoPO$_4$ and $\gamma$-NaCoPO$_4$ compounds by mechanochemical method and their characterization by X-ray powder diffraction patterns. These compounds are crystallized in the orthorhombic, hexagonal and monoclinic system, in $Pnma$, $P6_5$ and $P2_1/n$ space groups, respectively. The optical properties were measured by means of the UV-vis absorption spectrometry in order to deduce the absorption coefficient $\alpha$ and optical band gap $E_g$. The calculated values of the indirect band gaps ($E_g$) for three samples were estimated at 4.71 eV, 4.63 eV and 3.8 for compounds $\alpha$, $\beta$ and $\gamma$, respectively. The Tauc model was used to determine the optical gap energy of the synthesized compounds. Then, the results of the dielectric properties measured by varying the frequency are described.

1. Introduction

Phosphor materials have been discovered as phosphors, which combine with near-UV lighting chips in solid-state for use in white light-emitting diodes (LEDs). Among them, orthophosphates, with the general formula ABPO$_4$ (A: monovalent cation and B: divalent cation), have gained great interest in recent years, owing to their rich structural chemistry and potential applications in optics, ceramics, magnetic materials, ferroelectricity, catalysts etc.$^{1-3}$ The principle of the crystal structure of phosphate ABPO$_4$ depends on the nature of A and B metals. Thus, the oxygen coordination environment with a bivalent metal cation can be tetradra, pentahedra or octahedra, defining the olivine, tridymite, and maricite or zeolite type structure. For example, sodium cobalt(II) phosphate is commonly known in four different structures, as follows: the first is $\alpha$-NaCoPO$_4$ determined by Hammond and Barbier,$^6$ which crystallizes in the space group $Pnma$ composed of edge-sharing chains of CoO$_6$ octahedral cross-linked by PO$_4$ tetrahedral, and sodium ions Na$^+$, located in 10-coordinate cavities. The second polymorph is $\beta$-NaCoPO$_4$ (ref. 6) which belongs to the space group $P6_1$ and $P6_5$. This structure consists of P and Co atoms, occupying the tetrahedral sites while the Na atoms are located in the cavities of tetrahedral framework. The third polymorph ($\gamma$-NaCoPO$_4$), which crystallizes in the space group $P2_1/n$, has the same topology as that of zeolite ABW-type structure.$^7$ The phosphorus and the cobalt atoms are located in the tetrahedral site, while the sodium ones are located in the channels.

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To our knowledge, the physical properties of NaCoPO$_4$ are not reported in the literature. However, this compound is one of the ABPO$_4$-type of phosphate compounds which can be considered as an efficient host candidate for LEDs.

In fact, in this study, the three compounds $\alpha$-NaCoPO$_4$, $\beta$-NaCoPO$_4$ and $\gamma$-NaCoPO$_4$ are prepared by means of a mechanochemical method. The structure of the prepared samples is studied using an X-ray powder diffraction (XRD). The optical properties, under UV-visible irradiation, are reported. The main aim of this study is to determine some key optical parameters, such as, the optical energy gap ($E_g$), and the Urbach energy ($E_U$). In order to obtain an overview of the dielectric dispersion phenomenon, the dielectric properties, pertaining to the three phases ($\alpha$, $\beta$ and $\gamma$) in the frequency regime studied, are evaluated and then the results are correlated.

2. Experimental

2.1. Synthesis of material

The $\alpha$-NaCoPO$_4$, $\beta$-NaCoPO$_4$ and $\gamma$-NaCoPO$_4$ compounds were carried out via a mechanochemical method that uses a planetary ball mill.

The raw materials are: Na$_2$CO$_3$ (Sigma-Aldrich, 99%), Co$_2$O$_4$ (Sigma-Aldrich, $\geqslant$97%) and (NH$_4$)$_2$HPO$_4$ (Sigma-Aldrich, $\geqslant$99%).

The following reaction describes the synthesis of these compounds:

$$2\text{NH}_4\text{H}_2\text{PO}_4 + \text{Na}_2\text{CO}_3 + \text{Co}_2\text{O}_4 \rightarrow 2\text{NaCoPO}_4 + 2\text{NH}_3 + 3\text{H}_2\text{O} + \text{CO}_2$$

(1)

The appropriate amount of these reagents was weighed in stoichiometric ratio and well ground into a fine powder in an agate mortar.
The obtained powder was heated in an electric furnace, at a temperature of 573 K, for 8 h, in order to dislodge NH₃, H₂O, and CO₂.

After heating, the mixture was mechanically activated, using a planetary ball mill. To prevent the heating and sticking of the powder to the container walls and balls, and the powder agglomeration during the process, the milling sequence was selected, such as 10 min of milling, followed by 5 min of stop period. The experiments were performed using a hardened steel vial with five steel balls. The mixture of powders was milled for 12 h and the rotational speed was 500 rpm.

The obtained powder was compressed into cylindrical pellets, having a diameter of 8 mm, using a 3 ton per cm² uniaxial pressure to promote the reaction, before being heated at a temperature of 873 K for 4 days for \( \alpha \)-NaCoPO₄, 1023 K for 4 days for \( \beta \)-NaCoPO₄ and 1023 K for 5 days for \( \gamma \)-NaCoPO₄, then cooled slowly at a rate of 5 °C min⁻¹ at room temperature.

### 2.2. Characterization techniques

The crystalline properties were investigated at room temperature via an X-ray powder diffraction (XRD) that uses a Panalytical X’Pert ProDry powder diffractometer operating with CuKα radiation (\( \lambda_{\text{CuKα}} = 1.540600 \text{ Å} \), \( \lambda_{\text{CuKα}} = 1.544390 \text{ Å} \)) from 20 to 80 Bragg’s angle range. The unit cell parameters of the synthesized compounds were refined via the least square method powder data.

The optical properties were measured at room temperature, using a UV–3101PC scanning spectrophotometer that has a dual-beam monochromator, covering a spectrum from 200 nm to 2400 nm and using two sources: (i) xenon lamp for the UV-visible domain and (ii) halogen lamp for the infrared range. This technique makes it possible to determine the absorbance (A) and the reflectance (R). The optical absorption spectrum of the \( \alpha \)-NaCoPO₄, \( \beta \)-NaCoPO₄ and \( \gamma \)-NaCoPO₄ compounds was recorded at room temperature in powder; used in the form of films.

The dielectric measurements, performed in a wide range of frequency, were deduced from the admittance spectroscopy using an Agilent 4294A analyzer and Janis VPF800 cryostat. Before that, a thin Al layer with a disc shape was deposited on both sides of each sample. The amplitude of the applied alternative signal was fixed at 0.05 V.

### 3. Results and discussion

#### 3.1. X-ray diffraction measurements

The X-ray diffraction of \( \alpha \)-NaCoPO₄, \( \beta \)-NaCoPO₄ and \( \gamma \)-NaCoPO₄ compounds was carried out using a Panalytical X’Pert ProDry and then analyzed by Full Proof software. The pseudo-Voigt function was used for the simulation of the peak shapes. The refined parameters were: scale factor, zero shift, lattice constants, peak profile, asymmetry parameters, amplitudes of the modes transforming according to the irreps and independent isotropic atomic displacement parameters.

Room-temperature X-ray Diffraction (XRD) measurements were conducted over a 2θ range of 20°–100° for \( \alpha \)-NaCoPO₄ and a range of 20°–80° for \( \beta \)-NaCoPO₄ and \( \gamma \)-NaCoPO₄ oxide using a Cu-Kα source, as shown in Fig. 1(a)–(c).

All the reflection peaks, corresponding to 2θ values, were crystallized in the orthorhombic, hexagonal and monoclinic system, at room temperature, with space group \( \text{Pnnm}, \text{P6}_3 \) and \( \text{P2}_1/n \), respectively.

The quality factor, indicating the concurrence between the observed and the calculated profiles, was \( \chi^2 = 2.49, \chi^2 = 2.89 \) and \( \chi^2 = 3.14 \) respectively. The obtained reliability factors and lattice parameters of the three compounds, given in Table 1, are in good agreement with the published results.⁶⁻⁷

As can be clearly seen, Fig. 1(a)–(c) shows the appearance of other unidentified weak reflections due to the presence of impurities related to \( \text{Na}_2\text{Co}_3(\text{PO}_4)_2\text{P}_2\text{O}_7 \), red-NaCoPO₄ and \( \text{NaCo}_6(\text{PO}_4)_6 \) compounds.

#### 3.2. Structural description

The \( \alpha \)-NaCoPO₄ compound crystallizes in \( \text{Pnma} \) space group with cell parameters: \( a = 8.951(7) \text{ Å}, b = 6.891(8) \text{ Å}, c = 5.037(6) \text{ Å} \) and \( Z = 4 \). It consists of edge sharing chains of [CoO₆] octahedral parallel to the [010] direction, as shown in Fig. 2(a). These chains are cross-connected by the PO₄ tetrahedral, giving rise to large ten-coordinate cavities in which the Na⁺ ions are located. However, \( \beta \)-NaCoPO₄ compound was found to have a hexagonal system with a space group \( \text{P6}_3 \), the lattice parameters \( a = b = 10.174(1) \text{ Å}, c = 23.878(6) \text{ Å} \). The \( \gamma \)-NaCoPO₄ compound crystallizes in monoclinic system with a space group \( \text{P2}_1/n \), the cell parameters \( a = 5.243(6) \text{ Å}, b = 9.988(5) \text{ Å}, c = 7.471 (7) \text{ Å}, \beta = 90.210(4) \) and \( Z = 4 \). The structures of these compounds are built up of two types of tetrahedral PO₄ and CoO₄ corner-linked by common oxygen. The packing of MO₄ (M = P, Co) tetrahedral in this structure relatively delimits the large “tunnels” where the Na cations are located (Fig. 2(b and c)).

#### 3.3. Optical absorbance spectra

Optical properties are one of the most important factors to evaluate the light efficiency. Fig. 3 reveals the experimental UV–vis absorption spectrum of \( \alpha \)-NaCoPO₄, \( \beta \)-NaCoPO₄ and \( \gamma \)-NaCoPO₄ compounds in 200–800 nm wavelength range, at room temperature. The obtained spectra exhibit the nethermost energy absorption peaks at 209 nm, 211 nm and 210 nm, for \( \alpha \), \( \beta \) and \( \gamma \) compounds, respectively. These bands with maximum energies can be assigned to the absorption of the highest energetic level in the conduction band.

The absorption peak at 561 nm of the \( \alpha \)-NaCoPO₄ is attributed to \( 1\text{A}_1 \rightarrow 3\text{T}_1 \) transition and indicates the presence of CoO₆ octahedral. The \( \beta \)-NaCoPO₄ and \( \gamma \)-NaCoPO₄ compounds are characterized by the presence of peaks in the 400–460 nm range, attributed to \( 1\text{A}_1 \rightarrow 3\text{T}_2 \) transition, and bands in the 500–700 nm range assigned to the \( 4\text{A}_2 \rightarrow 4\text{T}_1 \) (P) transition for PO₄ tetrahedral.⁸⁻⁹ These results confirm the presence of the CoO₆ group in the \( \alpha \) phase and the CoO₆ group in the \( \beta \) and \( \gamma \) phases.

### 3.3.1. Direct and indirect optical band gap

The Kubelka–Munk method is used to analyze the reflection spectrum of the scattered light. It is widely used for semi-reflective materials in
Fig. 1  (a), (b) and (c) X-ray powder diffraction pattern of $\alpha$-NaCoPO$_4$, $\beta$-NaCoPO$_4$ and $\gamma$-NaCoPO$_4$ respectively: experimental data (the point symbols), calculated data (the solid lines), difference between them is shown at the bottom of the diagram Bragg positions are marked by vertical bar.
The value of the optical band gap \( E_g \) can be calculated using the following equation:

\[
E_g = \frac{1}{2} \left( \frac{c}{n} \right) \left( \frac{1}{\alpha} \right)
\]

The dependence of \((ahv)^2\) and \((ahv)^{1/2}\) on the photon energy for \(\alpha\), \(\beta\) and \(\gamma\) compounds is shown in Fig. 4. The intercepts of these plots on the energy axis denote the energy band gaps, since \(E_g = h\nu\) when \((ahv)^0 = 0\). The best fit is obtained for \(n = 1/2\); then the shapes of these curves favor the indirect transition. For these compounds the indirect gap energy is of the same order of \((4 \pm 0.03)\) eV (Table 2), thus these materials can be classified as wide gap semiconductors.

### 3.3.2 Urbach energies

The incorporation of impurity into the semiconductor often reveals the formation of band tailing in the band gap due to the interaction of phonons. The Urbach energy characterizes the disorder of a material and corresponds to transitions between extended states of the valence band and localized states of the conduction band. From the variation of the absorption coefficient, it is possible to deduce the disorder in the compound, given by this equation:

\[
\alpha = \alpha_0 \exp \left( \frac{h\nu}{E_U} \right)
\]

where \(\alpha_0\) is a constant and \(E_U\) is an energy, which is interpreted as the width of the tail of localized states in the forbidden band gap, \(\nu\) is the frequency of radiation, and \(h\) is Planck's constant.

### 3.3.3 The dispersion of the refractive index of the compounds

Firstly, the refractive index \(n\) of the sample is calculated from the gap energy using the following equation:

\[
n^2 - 1 = \frac{E_g}{20}
\]

The simplification of eqn (7) leads to:

\[
n^2 = \frac{3}{20} \left( \frac{E_g}{20} \right)
\]
The dispersive behavior of the refractive index \( n(\lambda) \) was deduced from the absorption data using the following equation:\(^{18}\)

\[
 n = \frac{(1 + R)}{(1 - R)} + \left[ \frac{(1 + R)}{(1 - R)} \right]^2 - (1 - k^2) \]

(9)

where \( R \) is the reflectance and \( k \) is the extinction coefficient.

The variation of refractive index \( n \) with the wavelength for \( \alpha \), \( \beta \) and \( \gamma \) compounds is illustrated in Fig. 6. The Cauchy's...
formula of the refractive index \( n \), as a function of the wavelength \( \lambda \), is: \(^{19,20}\)

\[
n = n_0 + \frac{A}{\lambda^2} + \frac{B}{\lambda^4},
\]

where \( n_0 \), \( A \) and \( B \) are the Cauchy’s parameters and \( \lambda \) is the wavelength.

According to the Cauchy distribution, the refractive index depends firstly on the material and secondly of the wavelength. The best fit of experimental data was added in Fig. 6.

The values of Cauchy’s parameters are gathered in Table 3.

Fig. 7 displays the variation of the absorption \( K \) indices for \( \alpha \), \( \beta \) and \( \gamma \) compounds. The extinction coefficient behavior of the sample tends to decrease with the wavelength increase. It should be noted that the values of \( A \) and \( B \) are negligible in the \( \gamma \)-NaCoPO\(_4 \) compound, indicating that the index \( n \) in this material is independent from the wavelength \( \lambda \).

### 3.4. Dielectric study

The complex permittivity formalism has been employed to reveal significant information about the physical behavior of the electrical and dielectric properties. It is described by a non-Debye model (Cole–Cole model) which gives the frequency dependent complex permittivity in the following form:\(^{21}\)

\[
\varepsilon_{cc} (\omega) = \varepsilon_{\infty} + \frac{\Delta\varepsilon}{1 + (i\omega \tau_{cc})^a} + \frac{\sigma_{dc}}{\varepsilon_{0} \omega}
\]

where \( \sigma_{dc} \) is the DC conductivity, \( \Delta\varepsilon = \varepsilon_{\infty} - \varepsilon_{\infty} \) is the dielectric strength, \( \varepsilon_{\infty} \) and \( \varepsilon_{\infty} \) are the high-frequency and static low-frequency limits of the real permittivity. The parameter \( a \), called Cole–Cole exponent, lies in the range from 0 to 1 and it is related to the width of the relaxation time distribution. Finally, \( \tau_{cc} \) is the characteristic time at which the dielectric loss of the given relaxation process is maximum.
The expressions of the real and imaginary parts of the dielectric complex permittivity are as follows:

\[
\varepsilon'(\omega) = \varepsilon_\infty + \frac{(\varepsilon_s - \varepsilon_\infty) \left[ 1 + \left( \frac{\omega}{\omega_1} \right)^{1-a} \cos \left( \frac{1-a}{2} \right) \right]}{1 + 2 \left( \frac{\omega}{\omega_1} \right)^{1-a} \cos \left( \frac{1-a}{2} \right) + \left( \frac{\omega}{\omega_1} \right)^{2(1-a)}} \]  

(12)

\[
\varepsilon''(\omega) = \frac{(\varepsilon_s - \varepsilon_\infty) \left( \frac{\omega}{\omega_1} \right)^{1-a} \sin \left( \frac{1-a}{2} \right)}{1 + 2 \left( \frac{\omega}{\omega_1} \right)^{1-a} \cos \left( \frac{1-a}{2} \right) + \left( \frac{\omega}{\omega_1} \right)^{2(1-a)}} + \frac{\sigma_{dc}}{\varepsilon_0 \omega} \]  

(13)

The first part in eqn (13) is related to the dipole reorientation polarization and the second part to the electrical conductivity.

The frequency dependence of real (\(\varepsilon'\)) parts of the dielectric constant at different temperatures are shown in Fig. 8(a–c). Based on this figure, it can be noted that no relaxation peaks are observed in the frequency range employed in this study. At low frequencies, as the temperature increases, \(\varepsilon'\) shows a dispersive behavior. Besides, the increasing value of \(\varepsilon'\) with increasing temperature may be attributed to the increase in space charge polarization process. On the other hand, at high frequencies, it approaches a limiting constant value \(\varepsilon_\infty(\omega)\), which can be interpreted as a result of a rapid polarization processes with no ionic motion contribution, because the frequency is too high and the ions can only oscillate without reaching the sample–electrode interface.

The dielectric loss spectrum, denoting the imaginary part \(\varepsilon''(\omega)\) of the complex permittivity, reveals the occurring dipolar molecular dynamic processes, with distinct origin processes appearing at diverse characteristic frequency ranges. At low

![Fig. 7 Dispersion curves of extinction coefficient k for the compounds as a function of wavelength.](image1)

![Fig. 8 (a, b and c) Frequency dependence of the real part of the dielectric constant, \(\varepsilon'\) at different temperatures for \(\alpha\)-NaCoPO₄, \(\beta\)-NaCoPO₄ and \(\gamma\)-NaCoPO₄ respectively.](image2)
frequency and high temperatures, the dielectric loss is predominantly Joule losses accompanied with charge conduction. The loss spectrum displayed bump-like features, corresponding to distinct reorientational processes.

The dielectric constant increases with the increase of the temperature due to the total polarization that arises from the dipole orientation and the trapped charge carriers. The dielectric dispersion rises drastically towards low frequencies and decays at higher frequencies.

The dielectric profile plot is higher at low frequencies possibly due to the different types of polarization effects. These effects may be caused by one or more contribution polarization factors, *i.e.*, electronic, atomic, ionic, interfacial factors etc. Higher dielectric constants at low frequencies depend on ionic vibration or movement, ion–ion orientation, and space charge effects. Thus, the higher value of $\varepsilon''$ in the low frequency region is probably due mostly to electrode polarization and space charge effects, confirming the non-Debye dependence. 23,24

It can be noted that dielectric constant $\varepsilon''$ of $\alpha$-NaCoPO$_4$, $\beta$-NaCoPO$_4$ and $\gamma$-NaCoPO$_4$ at $T = 600$ K have different values at a maximum of $\varepsilon''$, which is equal to 600, 2800, 2400, respectively. Hence, it can be concluded that the $\alpha$-phase has a low permittivity $\varepsilon''$ compared to the two other phases.

The conductivity values obtained by adjusting the curve $\varepsilon''$, using eqn (11), are plotted as a function of temperature (Fig. 10). The thermal evolution of the specific conductivity ($\log(\sigma) = f(1000/T)$) of $\alpha$, $\beta$ and $\gamma$ phases indicates an Arrhenius type behavior. The form of the curves indicates a discontinuity at the neighborhood of $T = 555$ K for the three

| Range of temperature | $T > 550$ K | $T < 550$ K |
|----------------------|-------------|-------------|
| $E_a$ (eV) of $\alpha$-NaCoPO$_4$ | 0.820 | 0.367 |
| $E_a$ (eV) of $\beta$-NaCoPO$_4$ | 0.756 | 0.126 |
| $E_a$ (eV) of $\gamma$-NaCoPO$_4$ | 0.804 | 0.220 |

Fig. 9(a–c) exhibits the frequency dependence of the imaginary dielectric constant $\varepsilon''$ for the three compounds. The dielectric constant increases with the increase of the temperature due to the total polarization that arises from the dipole orientation and the trapped charge carriers. The dielectric dispersion rises drastically towards low frequencies and decays at higher frequencies.

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Table 4 The values of the activation energy of permittivity

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compounds. The values of the energies of activation for \( \alpha \)-NaCoPO\(_4\), \( \beta \)-NaCoPO\(_4\) and \( \gamma \)-NaCoPO\(_4\) are, respectively: \( E_a = 0.820, 0.756, \) and 0.804 eV for \( T > 555 \) K and \( E_a = 0.36, 0.126, \) and 0.220 eV for \( T < 555 \) K (Table 4). The differential scanning calorimetry (DSC) study confirms the changes observed at \( \sigma_{dc} \) level by the presence of an endothermic peak near 555 K for the three phases (Fig. 11).

4. Conclusion

In this paper, the \( \alpha \)-NaCoPO\(_4\), \( \beta \)-NaCoPO\(_4\) and \( \gamma \)-NaCoPO\(_4\) monophosphates were prepared by a mechano-chemical method. First, the powder XRD study for the three compounds at room temperature revealed: the \( \alpha \)-NaCoPO\(_4\) crystallized in the orthorhombic system with \( Pnma \) space group, the values of the lattice parameters and volume were determined \( (a \approx 8.951 \text{ Å}, b \approx 6.891 \text{ Å}, c \approx 5.037 \text{ Å} \) and \( v = 310.688 \text{ Å}^3 \)); the \( \beta \)-NaCoPO\(_4\) crystallized in the hexagonal system with \( \text{P}6_3 \) space group, the values of the lattice parameters and volume were determined \( (a = b = 10.174 \text{ Å}, c = 2471.618 = A^3) \) and the \( \gamma \)-NaCoPO\(_4\) crystallized in the monoclinic system \( P2_1/n \) space group, the values of the lattice parameters and volume were determined \( (a = 5.243 \text{ Å}, b = 9.988 \text{ Å}, c = 7.471 \text{ Å} \) and \( v = 391.234 \text{ Å}^3 \)).

Second, the UV-vis spectroscopy was used to determine some of the key parameters, such as the absorption process at the absorption edge of \( \alpha \), \( \beta \) and \( \gamma \) phases, which revealed the absorption bands at \((209, 500, 561 \text{ nm}), (211, 415, 523 \text{ nm}) \) and \((210, 455, 535, 625 \text{ nm}) \), respectively. The Tauc model was used to determine the optical gap energy. The analysis of the data indicated the existences of optical indirect gaps, estimated to be 4.08 eV, 4.35 eV and 3.88 eV. The Urbach energies of these compounds were evaluated from these data. The \( \beta \)-NaCoPO\(_4\) compound has a low value of Urbach energy, confirming that this sample has the best crystal quality.

Finally, we investigated the dielectric properties at different temperatures for the \( \alpha \)-NaCoPO\(_4\), \( \beta \)-NaCoPO\(_4\) and \( \gamma \)-NaCoPO\(_4\) compounds. The dependence of the imaginary part of the complex permittivity rises sharply at low frequency, indicating that the electrode polarization and space charge effects have occurred, confirming the non-Debye dependence. The variation of dielectric constant and dielectric loss as a function of frequency was discussed. The temperature dependence on electrical conductivity \( \sigma_{dc} \) calculated from fitting \( \sigma_{dc} \) is described by an Arrhenius equation and characterized by a change of the slope at 555 K. This change is confirmed by the Differential scanning calorimetry.

Conflicts of interest

There are no conflicts to declare.

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