Regulation of Type 1 Inositol 1,4,5-Trisphosphate-gated Calcium Channels by InsP$_3$ and Calcium
Simulation of Single Channel Kinetics Based on Ligand Binding and Electrophysiological Analysis

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ABSTRACT Cytosolic calcium acts as both a coagonist and an inhibitor of the type 1 inositol 1,4,5-trisphosphate (InsP$_3$)-gated Ca channel, resulting in a bell-shaped Ca dependence of channel activity (Bezprozvanny I., J. Watras, and B.E. Ehrlich. 1991. Nature. 351:751–754; Finch, E.A., T.J. Turner, and S.M. Goldin. 1991. Science. 252:443–446; Iino, M. 1990. J. Gen. Physiol. 95:1103–1122). The ability of Ca to inhibit channel activity, however, varies dramatically depending on InsP$_3$ concentration (Combettes, L., Z. Hannaert-Merah, J.F. Coquil, C. Rousseau, M. Claret, S. Swillens, and P. Champeil. 1994. J. Biol. Chem. 269:17561–17571; Kaftan, E.J., B.E. Ehrlich, and J. Watras. 1997. J. Gen. Physiol. 110:529–538). In the present report, we have extended the characterization of the effect of cytosolic Ca on both InsP$_3$ binding and InsP$_3$-gated channel kinetics, and incorporated these data into a mathematical model capable of simulating channel kinetics. We found that cytosolic Ca increased the $K_a$ of InsP$_3$ binding $\sim$3.5-fold, but did not influence the maximal number of binding sites. The ability of Ca to decrease InsP$_3$ binding is consistent with the rightward shift in the bell-shaped Ca dependence of InsP$_3$-gated Ca channel activity. High InsP$_3$ concentrations are able to overcome the Ca-dependent inhibition of channel activity, apparently due to a low affinity InsP$_3$ binding site (Kaftan, E.J., B.E. Ehrlich, and J. Watras. 1997. J. Gen. Physiol. 110:529–538). Constants from binding analyses and channel activity determinations were used to develop a mathematical model that fits the complex Ca-dependent regulation of the type 1 InsP$_3$-gated Ca channel. This model accurately simulated both steady state data (channel open probability and InsP$_3$ binding) and kinetic data (channel activity and open time distributions), and yielded testable predictions with regard to the regulation of this intracellular Ca channel. Information gained from these analyses, and our current molecular model of this Ca channel, will be important for understanding the basis and regulation of intracellular Ca waves and oscillations in intact cells.

KEY WORDS: cerebellum • inositol 1,4,5-trisphosphate receptor • intracellular calcium channel • calcium signaling • kinetic model

INTRODUCTION

The inositol 1,4,5-trisphosphate (InsP$_3$)$_1$-gated Ca channel plays a critical role in the regulation of intracellular Ca concentrations after hormonal activation of the phosphoinositide cascade in a wide variety of cell types (Abdel-Latif, 1986; Berridge and Irvine, 1989; Clapham, 1995). The mechanisms underlying regulation of the InsP$_3$-gated channel are poorly understood; however, the involvement of both cytosolic Ca and InsP$_3$ in the regulation of this channel is well established (Iino, 1990; Payne et al., 1990; Bezprozvanny et al., 1991; Finch et al., 1991; Bootman et al., 1995; Kaftan et al., 1997). That is, InsP$_3$ is absolutely required for the opening of the channel, though channel activity can be modified by cytosolic Ca. Elevating the cytosolic Ca concentration from 0.01 to 0.3 $\mu$M in the presence of 2 $\mu$M InsP$_3$, for example, resulted in a dramatic increase in channel activity (Bezprozvanny et al., 1991). Further elevation of cytosolic Ca, however, decreased channel activity, with near complete inhibition of the channel in the presence of 5 $\mu$M Ca (Bezprozvanny et al., 1991). Three basic models have been proposed to explain this bell-shaped Ca dependence of the channel differing in terms of the effects of InsP$_3$ on the bell-shaped Ca dependence. In one model (Bezprozvanny, 1994), the peak of the bell-shaped Ca dependence is unaffected by InsP$_3$ concentration. The other two models predict either a shift to the left (Tang et al., 1996) or the right (De Young and Keizer, 1992) in the peak of the bell-shaped Ca dependence of channel activity as InsP$_3$ concentrations increase.
Recent studies indicate that the InsP$_3$ concentration influences the Ca dependence of InsP$_3$-induced Ca release, with an increased sensitivity to Ca-dependent inhibition occurring at low InsP$_3$ concentrations (Hannaert-Merah et al., 1995; Kaftan et al., 1997). Thus, the peak of the bell-shaped Ca dependence of InsP$_3$-gated channel activity shifted to the right as InsP$_3$ concentration was increased from 0.2 to 2 μM (Kaftan et al., 1997). Further elevation of InsP$_3$ concentration to 180 μM overcame the Ca-dependent inhibition of channel activity (Kaftan et al., 1997), which may reflect the presence of a second low affinity InsP$_3$ binding site on the channel complex. Recently, we modeled this complex steady state behavior of the InsP$_3$-gated channel by extending a basic 8-state model proposed previously (De Young and Keizer, 1992) to 16-states, assuming that there are two InsP$_3$ (with dissociation constants of 0.3 and 10 μM) and two Ca binding sites per InsP$_3$ receptor in the tetrameric channel complex (Kaftan et al., 1997). In the present report, we explored in further detail the Ca dependence of InsP$_3$ binding, as well as the influence of Ca and InsP$_3$ on the mean open times of the InsP$_3$-gated channel, and incorporated these data into a novel mathematical model of the channel. The proposed model differs conceptually from previous models in that it focuses on the tetrameric channel complex as a unit, but more importantly it provides a better fit of the steady state channel and binding data, and simulates the kinetics of channel activation.

**Methods**

**Isolation of Microsomes**

Microsomes were isolated from canine cerebellum, as described previously (Watras et al., 1991). To minimize proteolysis, all solutions used for the isolation/storage of the cerebellar microsomes included a protease inhibitor cocktail (5 μg/ml leupeptin, 2 μg/ml aprotenin, 1 μg/ml pepstatin A, 0.1 mM PMSF). In brief, cerebellum was homogenized in 6 vol of buffer A (20 mM HEPES, 0.1 mM EGTA, 5 mM Na$_2$HPO$_4$, pH 7.2, 4°C) using a Brinkman polytron. The suspension was centrifuged at 4,000 g for 20 min, and the supernatant was centrifuged at 100,000 g for 30 min. The pellet from the latter centrifugation was resuspended in 3 vol of buffer B (20 mM HEPES, 0.6 mM KCl, 20 mM Na$_2$PO$_4$, 5 mM NaNCl, pH 7.2, 4°C), and then centrifuged at 4,000 g for 20 min. The resulting supernatant was centrifuged at 100,000 g for 30 min. The final pellet was resuspended in buffer C (10 mM MOPS, 10% sucrose, pH 7.0) to a protein concentration of ~6 mg/ml (as determined using a protein assay kit; Bio-Rad Laboratories; Bradford, 1976), quick frozen in liquid nitrogen, and stored at −80°C.

**InsP$_3$ Binding**

InsP$_3$ binding was determined by a centrifugation technique (Benevolseny et al., 1994), using buffer identical to that used for the InsP$_3$-gated channel activity measurements (Bezprozvanny et al., 1991). Binding media contained 250 mM HEPES, 110 mM Tris, 1 mM ATP, 0.5 mM EGTA, pH 7.35, 0.6–1,200 nM $^{3}H$-InsP$_3$, and CaCl$_2$ (to yield the specified free Ca concentrations). InsP$_3$ binding was initiated by addition of cerebellar membranes to the above buffer. After an 8-min incubation, InsP$_3$ binding was terminated by centrifugation (40,000 g for 10 min). The supernatant was removed by aspiration. The pellets were dissolved in Soluene 350, and then assayed for radioactivity by liquid scintillation counting. Nonspecific binding was determined in the presence of 40–160 μM nonradioactive InsP$_3$. Scatchard analysis of InsP$_3$ binding was performed using an iterative curve-fitting routine for two binding sites (SigmaPlot; Jandel Scientific). All binding studies were replicated three to five times, with different microsomal preparations.

Calculations of total Ca needed to obtain a specified free Ca concentration were based on previously published association constants (Fabio, 1988), adjusted to pH 7.35 (at the specified temperature; 0°C or 22°C). The apparent association constants (M$^{-1}$) for Ca-EGTA and Ca-ATP used for these calculations were 1.055 × 10$^4$ and 7.595 × 10$^3$, respectively, at 0°C, and 1.244 × 10$^3$ and 6.312 × 10$^3$, respectively, at 22°C.

**Measurement of Channel Activity**

InsP$_3$-gated channel activity was measured as described previously (Bezprozvanny et al., 1991; Kaftan et al., 1997), using 53 mM Ba in the trans chamber as current carrier. The planar lipid bilayer contained phosphatidylethanolamine and phosphatidylserine (3:1 wt:wt; Avanti Polar Lipids), dissolved in decane (20 mg/ml). Cytosolic bilayer solutions contained 500 μM Na-ATP, 500 μM EGTA, 110 mM Tris, and 250 mM HEPES, pH 7.35. Luminal solutions contained 53 mM Ba(OH)$_2$, 250 mM HEPES, pH 7.35. Calibrated CaCl$_2$ was added to the cytoplasmic solution to obtain the desired free Ca concentration (Fabio, 1988). The free Ca concentration was checked by spectrofluorometric measurements using BTC (Molecular Probes, Inc.). InsP$_3$-gated channel activity was initiated by addition of InsP$_3$ at the specified concentration. The number of channels in each experiment was estimated from the maximum number of channels observed simultaneously in the bilayer (Horn, 1991). The InsP$_3$ dependence of the open probability, measured at a fixed Ca concentration, was used to correct for variations in the maximum open probability among individual channels. Transmembrane voltage was maintained at 0 mV and the single channel current was amplified (Warner Instruments) and stored on VHS tape (Instrutech Corp.). Data were filtered at 1 kHz and digitized at 5 kHz for computer analysis using pClamp 6.0 (Axon Instruments).

**Modelling**

Modeling InsP$_3$-gated channel activity was done by considering the tetrameric channel complex as one functional unit having four medium affinity InsP$_3$ binding sites (K$_d$ = 0.3 μM at 22°C), four low affinity InsP$_3$ binding sites (K$_d$ = 10 μM at 22°C), and four Ca binding sites. The mathematical model assumes mass action kinetics with first order on (k$_+$) and off (k$_-$) rates for the binding of any ligand (L) to a specific site on the receptor monomer subunit (R), which was described by ordinary differential equations of the form:

\[
\frac{d[R]}{dt} = k_+ [R][L] - k_- [RL]
\]

At equilibrium, the distribution of the receptor states is a function of the ligand dissociation constant (K$_d$ = k$_-$/k$_+$) and free concentration of ligand. The four InsP$_3$ receptor subunits comprising the channel complex were considered identical and positionally equivalent, and a state transition reaction scheme was constructed for the 125 possible states of the channel tetramer complex (T) (see RESULTS). The various K$_d$ values fully define...
the steady state distribution of states and allowed us to calculate the relative abundance \( t_{i,c,j} = \frac{[T_{i,c,j}]}{[T}_{\text{total}} \) (of tetramers with \( i \) and \( j \) InsP\(_3\) molecules bound to the medium and low affinity site, respectively, and \( c \) Ca molecules bound) by solving a linear system of first degree equations that result from the equilibrium condition for formation/dissociation of each state. The no-flux equilibrium condition, as well as several assumptions regarding binding interactions, were used to constrain the various dissociation constants that were not directly inferred from binding experiments (see Results). Channel states characterized by the binding of one to two Ca and two to four InsP\(_3\) molecules were assumed to be “active,” i.e., exhibit a high open probability. InsP\(_3\) binding to the low affinity site was assumed to create an active state, independent of InsP\(_3\) and/or Ca binding to other sites within the channel complex. Channel activity was described as a transition between two substates, open and closed (Scheme I). First order reaction rates were assumed for both transitions, and the resulting open probability for any given state of the channel is:

\[
P_{\text{open}}(t) = \frac{\alpha_{i,c,j}}{\alpha_{i,c,j} + \beta_{i,c,j}}.
\]

Iterative curve-fitting of the InsP\(_3\)-gated Ca channel open probability data given the Ca dependence of InsP\(_3\) binding using a standard quasi-Newtonian algorithm with forward differencing and quadratic extrapolation was then performed to determine the values of unknown parameters. The open time histograms were used to further constrain the model and facilitate kinetic simulations. Diffusion-limited on rates of binding were assumed in all steps for both Ca and InsP\(_3\) binding and each off rate was determined by multiplication with the respective dissociation constant. Channel opening and closing rates were determined from the open probabilities of the respective active states given the constraints imposed on closing rates in order to match the experimental distribution histogram of open states. Simulations of the single channel recordings were performed by stochastic modeling of state transition events of the channel complex, using a Markovian model of probability matrix decomposition (Colquhoun and Hawkes, 1983) to predict state transitions over a given time period. The behavior of the channel is calculated from the matrix differential equation:

\[
dP(t)/dt = P(t)Q,
\]

where the elements \( p_{m,n}(t) \) of the matrix \( P(t) \) are the probabilities of a channel to get from state \( m \) to \( n \) over the time period \( t \) and the elements of the matrix are the rates of transition from state \( m \) to \( n \). The solution of this equation is:

\[
P(t) = e^{Qt}I + Q \frac{(e^{Qt} - I)}{Q} = I + Q t + \frac{Q^2 t^2}{2!} + \frac{Q^3 t^3}{3!} + \ldots \]

where \( I \) is a unit matrix. Relaxation from a random state (picked according to steady state distribution probability) was simulated for the desired time length to obtain channel state data sets at the chosen time step. Predicted traces were generated for the simultaneous presence of up to 10 channels in the membrane from individual current functions \( i(t) = A \cdot \chi(t) + S(t) \), where \( A \) is the current amplitude through the open channel, \( \chi(t) \) is either 0 or 1, depending on whether the channel is in one of the closed or one of the open states, respectively, and \( S(t) \) is a standardized noise spectrum function chosen to match the experimentally observed noise in any given trace.

Results

Ca Inhibition of InsP\(_3\) Binding

There have been conflicting reports on the influence of Ca on InsP\(_3\) binding. Initial reports indicated that micromolar Ca concentrations could completely inhibit InsP\(_3\) binding, with half-maximal inhibition occurring at 0.3 \( \mu \)M Ca (Worley et al., 1987; Supattapone et al., 1988). On the other hand, Ca-dependent inhibition of cerebellar membranes can also occur as an artifact resulting from activation of an endogenous phospholipase C (Mignery et al., 1992). We have re-investigated the influence of Ca on InsP\(_3\) binding, with the goal of relating Ca-dependent modulation of InsP\(_3\) binding to the bell-shaped Ca dependence of channel activity. As shown in Fig. 1A, micromolar Ca decreased InsP\(_3\) binding when using media identical to that used for channel activity measurements. Ca concentrations as high as 100 \( \mu \)M resulted in only partial inhibition of InsP\(_3\) binding (Fig. 1A, filled bars), in contrast to the near complete inhibition previously reported (Worley et al., 1987). The inhibitory effects of Ca on InsP\(_3\) binding were reversed by addition of EGTA (Fig. 1A, hatched bars), ruling out contributions of Ca-dependent activation of an endogenous phospholipase C (Mignery et al., 1992; Benevolensky et al., 1994). Moreover, the presence of 100 \( \mu \)M free barium, an inhibitor of phospholipase C (Benevolensky et al., 1994), did not alter this Ca-dependent inhibition of InsP\(_3\) binding (data not shown).

Scatchard analyses of InsP\(_3\) binding (Fig. 1B) indicated that this decreased InsP\(_3\) binding was attributable to a Ca-dependent increase in the \( K_d \) for InsP\(_3\) binding. The Scatchard plots were nonlinear, suggesting the presence of multiple InsP\(_3\) binding sites. Data (which were obtained over an InsP\(_3\) concentration range of 1–600 nM) could be fit assuming two InsP\(_3\) binding sites (with \( K_d \) values of 1 and 50 nM in the absence of Ca). The concentration of InsP\(_3\) used was too low to observe the low affinity InsP\(_3\) binding site discussed below (Kaftan et al., 1997). The 50-nM binding site was abundant, representing 99% of the total sites in the absence of Ca. As the Ca concentration was increased from 0.0004 to 10 \( \mu \)M, the apparent \( K_d \) for this site increased 3.5-fold (Fig. 1, B and C). Half maximal inhibition occurred at 0.3 \( \mu \)M Ca with a Hill coefficient of 1.5. The high affinity InsP\(_3\) binding site, by contrast, was in very low abundance, representing <1% of the total binding at all Ca concentrations examined, and its \( K_d \) (1 nM) appeared to be Ca independent (consistent with our previous observations in aortic smooth muscle membranes; Benevolensky et al., 1994).
To more closely resemble the conditions used for channel activity determinations, InsP₃ binding assays were repeated at room temperature again using media identical to that employed in the single channel experiments. Increasing the temperature to 22°C resulted in a 67% reduction in InsP₃ binding; an inhibition that was reversed by reducing the temperature to 0°C (Fig. 2 A). Scatchard analyses of InsP₃ binding at 0°C and 22°C (Fig. 2 B) show that the increase in temperature results in a decrease in InsP₃ binding affinity, with no apparent effect on the maximal number of InsP₃ binding sites. The calculated Q₁₀ for this temperature-dependent change in InsP₃ binding affinity was 2.3, consistent with that calculated for InsP₃ binding to rat basophilic leukemia cells (Watras et al., 1994).

The Ca dependence of InsP₃ binding was also reexamined at 22°C (Fig. 3), and yielded results similar to those observed at 0°C (Fig. 1). As shown in Fig. 3 A, micromolar Ca concentrations reduced InsP₃ binding (measured in the presence of 170 nM InsP₃) by 55% (■), and this inhibition was completely reversed by Ca chelation with EGTA (□, dotted line). Increasing the Ca concentration to 100 μM did not increase the extent of the inhibition (data not shown), consistent with our previous observations in aortic smooth muscle microsomes (Benevolensky et al., 1994). The Ca-dependent inhibition at 22°C showed a high level of cooperativity (Hill coefficient, 2.8; half-maximal inhibition at 0.45 μM Ca) (Fig. 3 A), and was attributable to a Ca-dependent increase in the Kₐ for InsP₃ binding (Fig. 3 B). The Kₐ for InsP₃ binding at 22°C increased from 0.30 (at 0.0005 μM Ca; ○) to 1.78 μM in the presence of a high Ca concentration (●; 50 μM free Ca) (Fig. 3 B). There was no evidence for an effect of Ca on the maximum number of InsP₃ binding sites at either 0°C or 22°C.

The Scatchard analyses in Figs. 2 and 3 show the presence of only one InsP₃ binding site (Kₐ = 50 nM at 0°C and 312 nM at 22°C) due to the range of InsP₃ concentrations used (5 nM–1 μM), where neither the high (Kₐ = 1 nM) nor the low (Kₐ = 10 μM) affinity site can be resolved. These sites are observed only if one extends the InsP₃ concentration range below 1 nM (as in Fig. 1) and above 5 μM (Kaftan et al., 1997). Three InsP₃ binding sites were observed in cerebellar microsomes and purified InsP₃ receptor preparations, purified by either heparin-agarose chromatography or immunoprecipitation (Kaftan et al., 1997). In all assays, the 1-nM InsP₃ binding site was a minor component, whereas the medium and low affinity InsP₃ binding sites were abundant. At 0°C, the calculated dissociation constants for InsP₃ binding to these two predominant InsP₃ binding sites were 50 nM (medium affinity site) and 10 μM (low affinity site) (Kaftan et al., 1997). At 22°C, the dissociation constant of the 50-nM site increased to ∼300 nM.

Figure 1. Micromolar Ca inhibits InsP₃ binding to cerebellar membranes by increasing the Kₐ for InsP₃. (A) InsP₃ binding decreased 66% when the Ca concentration was increased from 0 to 100 μM (solid bars), and this inhibition was fully reversible upon chelation of Ca by EGTA (hatched bars). The InsP₃ concentration was 10 nM. One of three similar experiments. (B) Scatchard analysis indicated that Ca decreased InsP₃ binding affinity without a change in maximal binding. Concentrations of Ca tested were 0.0004 (○), 0.1 (△), 0.5 (■), and 10 (▲) μM. Note that complete inhibition of InsP₃ binding was not observed. (C) The Kₐ values from B plotted as a function of the Ca concentration for two experiments (○ and △). The Ca-dependent increase in the Kₐ for InsP₃ binding increased 3.5-fold over the Ca concentration range tested with half maximal increase at 0.3 μM Ca (data were fit using a Hill equation with a coefficient n = 1.5).
whereas the dissociation constant for the 10-μM InsP3 binding site could not be accurately ascertained. It appeared to remain in the 10-μM range, suggesting that the low affinity InsP3 binding site was largely temperature insensitive.

InsP3 Dependence of Channel Activity

We previously reported that the Hill coefficient for InsP3-induced Ca release was 1.3, whereas the single channel activity determinations suggested a Hill coefficient 1.0 (Watras et al., 1991). The previous experiments underestimated the Hill coefficient because the lowest concentration of InsP3 used activated the channel to 10% of the maximum, a level of activity too high for accurate measurements of cooperativity. Reinvestigation of the channel activity at lower InsP3 concentrations indicate that the Hill coefficient for channel activity measurements is at least 1.7 (Fig. 4). This value for the Hill coefficient may reflect the requirement for InsP3 to bind to at least two of the four InsP3 receptors to activate the channel.

Open-Time Distribution of InsP3-gated Channels

Open-time histograms of InsP3-gated channels at two different cytoplasmic Ca concentrations were fit assuming an exponential with two time constants (Fig. 5). Increasing the number of time constants to three did not statistically improve the fit. In the presence of 0.01 μM Ca and 2 μM InsP3 (Fig. 5 A), the appropriate time constants were 1.8 and 9.3 ms. As the Ca concentration was increased to 0.1 μM (Fig. 5 B), the time constants decreased to 0.6 and 4.7 ms. Thus, the channel open
times are Ca dependent. Similar analyses were done at a number of Ca and InsP$_3$ concentrations, with the appropriate time constants incorporated into the mathematical model described below. Based upon the observed value for the Hill coefficient (1.7), the model was constrained to require the binding of two molecules of InsP$_3$ to open the channel.

Modelling Channel Activity Data and InsP$_3$ Binding

Recent studies indicate that the cerebellar InsP$_3$-gated Ca channel exhibits a complex regulation by Ca and InsP$_3$ (Kaftan et al., 1997). Data points from this earlier report are shown in Fig. 6; lines through the points represent the fit using the model described in the present report (Fig. 6 A). For comparison, the fit obtained using the 16-state model (Kaftan et al., 1997) is also shown (Fig. 6 B), but fails to accurately predict channel activity at low InsP$_3$ concentrations. The current model provides an excellent fit of the channel data over a broad range of InsP$_3$ and Ca concentrations.

Simple mass-action kinetics was assumed for ligand binding to the sites on the receptor monomer subunits (see Methods). Since the functional unit of the channel is the tetrameric complex (T), this analysis was extended by introducing apparent dissociation constants for sequential binding to the four monomer subunits. A total of $2^4 = 16$ possible different states of the channel can be generated by binding of up to four ligand molecules to the same site on the four different monomer subunits of the tetramer. We considered the subunits identical and positionally equivalent, which reduces the 16 states to only 5 different states according to Scheme II.

\[ T \xrightleftharpoons{4k_1}{k_1^-} TL \xrightleftharpoons{3k_2}{2k_2^-} TL_2 \xrightleftharpoons{2k_3}{3k_3^-} TL_3 \xrightleftharpoons{k_4}{4k_4^-} TL_4 \]

(scheme II)

The resulting apparent dissociation constants for sequential binding are:

\[
K_{d1}' = \frac{1}{4} K_{d1}, \quad K_{d2}' = \frac{2}{3} K_{d2}, \quad K_{d3}' = \frac{3}{2} K_{d3}, \quad K_{d4}' = 4 K_{d4}.
\]

This general framework was applied to InsP$_3$ and Ca binding to the channel complex, assuming that each monomer in the tetrameric channel complex contains the equivalent of one Ca regulatory site (C), one medium affinity InsP$_3$ site (I), and one low affinity InsP$_3$ site (J). This results in five different states of the tetrameric channel complex (zero, one, two, three, or four sites occupied) for each of the three classes of sites (C, I, and J). A total of $5^3 = 125$ different states per channel complex are predicted ($T_{i,c,j}$, where i, c, and j

Figure 4. The InsP$_3$ dependence of channel activation. The open probability of single InsP$_3$-gated channels was plotted as a function of the InsP$_3$ concentration. Cytosolic Ca concentration was fixed at 0.16 \( \mu \text{M} \). Constants obtained from the fit (Hill equation) were incorporated into the mathematical model described below. Based upon the observed value for the Hill coefficient (1.7), the model was constrained to require the binding of two molecules of InsP$_3$ to open the channel.

Figure 5. Single channel open times decrease as Ca concentration is elevated from 0.01 (A) to 0.1 (B) \( \mu \text{M} \) Ca. These panels are representative of the analyses done over a range of Ca and InsP$_3$ concentrations. At least two classes of open times were evident at each calcium concentration. Curve fits were biexponential decays with time constants of 1.8 and 9.3 ms (A; 2:1 weighting) and 0.6 and 4.6 ms (B; 1:1 weighting).
represent the number (zero to four) of ligand molecules bound to the I, C, and J sites, respectively. Fig. 7 shows the state transition scheme for the 25 states in the absence of InsP$_3$ binding to the low affinity site (T$_{i,c,0}$). The apparent dissociation constants of binding of InsP$_3$ to the I site were labeled $K_{d,i}$ (for a tetramer that has i other I sites and c of the C sites occupied) and of Ca binding to the C site were labeled $K_{d,c}$ (for a tetramer that has c other C sites and i of the I sites occupied). This reaction scheme was extended upwards by drawing four additional planes to include binding to the low affinity InsP$_3$ binding site (J).

The "gating" or "regulatory" action of ligand binding to the various sites on the channel is in effect determined by the differences in the opening/closing transition rates of the different states (see methods; i.e., a state with $\alpha = 0$ is an "inactive" state). Essentially, "active" states were hypothesized to be channels having either two or more medium affinity InsP$_3$ sites and one or two Ca sites occupied (Fig. 7, highlighted states; a total of eight active states in the absence of binding to the J site). Additionally, active states were channels having two or more low affinity InsP$_3$ sites (I) and any number of Ca sites occupied (in upper planes of the full 125-state model, not shown in Fig. 7). The activation of the channel through J was thus assumed to overcome Ca-dependent inhibition of the channel, consistent with experimental observations (Kaftan et al., 1997).

At any given Ca and InsP$_3$ concentration, the only parameters needed to calculate the steady state relative distribution of the different states and the overall channel open probability were the various apparent dissociation constants $K_{d,i}^{C}$, $K_{d,c}^{I}$, and $K_{d,j}^{J}$.

And the open probabilities of the various states $P_{o}^{(i,c)}$. Some of these parameters could be inferred from measured dissociation constants based on several assumptions and constraints. In accordance with the thermodynamic principle of detailed equilibrium (Hille, 1992), reaction rates between any combination of states that form a complete cycle (e.g., the highlighted set of four transitions in Fig. 7) were constrained to yield no net flux at equilibrium. Thus, the apparent dissociation constants ($K_{d}^{(i,c)}$) of binding to the C and I site were constrained as follows:

$$K_{d,i}^{C}, K_{d,c}^{I}, and K_{d,j}^{J},$$

With regard to interactions when binding to the same site on different monomer subunits, we assumed that Ca binding is cooperative ($K_{d,i}^{C} > K_{d,c}^{I}$), whereas InsP$_3$ binding is independent $K_{d,i}^{C} = K_{d,c}^{I}$; for simplicity, we assumed that the cooperative effect is the same for each step during sequential binding of Ca; i.e., the ratio $K_{d,i}^{C} > K_{d,c}^{I}$ is the same for $c = 0...3$ (the value of this ratio is a parameter we named cooperativity factor, $K_{d,C}$). The dissociation constants for InsP$_3$ were derived directly from the binding data (Fig. 1 C, and Table I). For the I site, we used $K_{d,i}^{C} = 0.3 \mu M$ (no Ca bound) and $K_{d,c}^{I} = 1.05 \mu M$ (for $c > 0$, reflecting the non-competitive inhibition of InsP$_3$ binding by Ca). Binding of InsP$_3$ to the low affinity site appears independent of binding to any other sites with a dissociation constant $K_{d}^{C} = 10 \mu M$. Given the above constraints and InsP$_3$ binding parameters, all the dissociation constants for Ca binding could be derived from only two parameters, $K_{d,i}^{C}$ and $K_{d,C}$. The values of these as well as of $P_{o}^{(i,c)}$ were obtained through standard curve-fitting algorithms for the predicted channel open probability data (Table I). The predicted $K_{d}^{C}$ of Ca binding to the first site is $0.7 \mu M$, which approximates the reported $K_{d}^{C}$ for Ca binding to a cytoplasmic region of the type 1 InsP$_3$ receptor (Sienaert et al., 1996). Table I summarizes all the parameters used to construct the model.
Simulation of Single Inositol 1,4,5-Trisphosphate–gated Channels

A sample recording of InsP₃-gated channel activity obtained in the presence of 0.2 mM InsP₃ and 0.1 mM Ca (Fig. 8 A) is shown for comparison with channel activity predicted by the model (B). Using constants derived from the InsP₃ binding analyses, channel open time histograms, and the steady state open probability data, the mathematical model described above was used to generate a time course of channel activity in the presence of 0.2 mM InsP₃ and 0.1 mM Ca. The predicted channel activity data (Fig. 8 B) closely resemble the actual channel recording (A); moreover, quantitative comparisons show that the dwell time histogram of a simulated trace (Fig. 8 C) could be fitted with a double exponential curve using identical time constants as those used to fit the experimental data obtained at the same Ca and InsP₃ concentrations (Fig. 5 B).

The parameter list used for the steady state analysis (and values) is not sufficient to calculate the values re-
quired to fill the transition rate matrix (see Methods). This requires explicit numbers for the on and off rates ($k_1$ and $k_2$ values) and opening and closing rates ($\alpha$ and $\beta$ values). The on rates for binding were based assuming diffusion limitation for both Ca and InsP$_3$ (10 and 250 $\mu$M$^{-1}$s$^{-1}$, respectively; this includes the effect of buffering for Ca) binding. The channel closing rates were based on the single channel open time distribution histograms. A minimum of two different closing rates is demonstrated by the biexponential fits of the dwell times. To accurately predict the apparent time constants and relative ratios, as well as their change with increasing Ca concentration (Fig. 5), we used four different closing rates ranging from 150 to 1,000 s$^{-1}$ (Table I) whereby the faster rates were assigned to the active states with two Ca bound and the slower rates to the active states with one Ca bound. The corresponding binding off rates and channel opening rates were then calculated using the parameter values from the steady state simulations:

$$k^1_{i,c} = K^1_{d_{i,c}} \cdot k^1_{i,c}; \quad k^C_{i,c} = K^C_{d_{i,c}} \cdot k^C_{i,c};$$

$$\alpha_{i,c} = \beta_{i,c} \cdot \frac{P^\text{open}_{i,c}}{1 - P^\text{open}_{i,c}}.$$

To maintain the necessary matrix algebra at a manageable size, we limited ourselves to simulations of channel activity under conditions with $[\text{InsP}_3] \leq 2 \mu$M, so that the effect of the J site on channel activity is negligible and only the 25 states depicted in Fig. 7 (and the corresponding substates of the active states) have to be included in the calculations.

To produce simulated traces of channel current recording, we generated predicted relaxation data. An initial state was chosen for time 0, either arbitrarily or the most probable state for the given Ca and InsP$_3$ concentration (as indicated by the steady state distribution values). We calculated the probability matrix $P(t)$ for a

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**Table I**

| Model Parameters |
|------------------|
| **InsP$_3$ binding** |
| Medium affinity site | $K^d_{d_{i,c}}$ 0.3 $\mu$M |
| Low affinity site | $K^d_{d_{i,c}}$ (c > 0) 1.05 $\mu$M |
| On rates | $k^1_{i,c}, k^C_{i,c}$ 250 $\mu$M$^{-1}$s$^{-1}$ |
| **Ca binding** |
| For first molecule | $K^C_{d_{i,c}}$ 0.7 $\mu$M |
| Cooperativity factor | $K_{K_{Ca}}$ 2.6 |
| On rates | $K^C_{d_{i,c}}$ 10 $\mu$M$^{-1}$s$^{-1}$ |
| **Channel activity** |
| Open probabilities | $P^\text{open}_{i,c,0}$ (c = 1; i = 1...4) 0.04...0.13 |
| $P^\text{open}_{i,c,j}$ (j > 1) 0.033 |
| Opening rates | $\alpha_{i,c,j}$ 2...40 s$^{-1}$ |
| Closing rates | $\beta_{i,c,j}$ 150...1000 s$^{-1}$ |

See Fig. 7 and text for notation.

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**Figure 8.** Comparison of single channel currents in the presence of 0.2 $\mu$M InsP$_3$ and 0.1 $\mu$M free Ca. A represents an experimentally measured channel recording, whereas B represents a simulation, generated from the current mathematical model. C shows a dwell-time histogram obtained from 5 min of the simulated trace from which a representative stretch is shown in B. The open time distribution is accurately fit by a biexponential curve using the same parameters as for the experimental data shown in Fig. 5 B.
time value equal to the chosen sampling interval in single channel records ($\tau = 40 \mu s$), and generated data sets of predicted channel states at the given sampling rate for a desired length of simulation. Fig. 8B shows a representative segment of a simulated trace with 2.1 pA open channel current amplitude and normally distributed baseline noise of 1 kHz median frequency.

The current mathematical model is thus capable of modeling both steady state open probability data, ligand binding data, and channel kinetics.

discussion

Recent studies in our laboratory indicate that Ca and InsP$_3$ interact to increase the dynamic range of the InsP$_3$-gated Ca channel (Kaftan et al., 1997). At a resting intracellular Ca concentration of 0.05-0.1 $\mu$M, agonist-induced production of InsP$_3$ would be expected to activate the InsP$_3$-gated Ca channel, with a subsequent rise of intracellular Ca (up to 0.3 $\mu$M) promoting further activation of the channel through a positive feedback mechanism (Iino, 1990; Bezprozvanny et al., 1991; Finch et al., 1991). Negative feedback of Ca on the InsP$_3$-gated channel, however, will limit the rise of intracellular Ca, with near complete inhibition of the channel at 5 $\mu$M Ca, even in the presence of 2 $\mu$M InsP$_3$ (Bezprozvanny et al., 1991). Increasing the InsP$_3$ concentration results in a rightward shift in the bell-shaped curve (Kaftan et al., 1997). Thus, the channel is more sensitive to the inhibitory effects of Ca when the InsP$_3$ concentration is low. This may be important physiologically, as it would further limit the rise in intracellular Ca in the presence of low InsP$_3$ concentrations. That is, it would promote a more gradual rise in intracellular Ca concentration over the InsP$_3$ concentration range 0.02-2 $\mu$M. Conversely, very high InsP$_3$ concentrations can largely overcome this Ca-dependent inhibition of the channel (Kaftan et al., 1997), preventing closure of the channel in local/confined areas such as those near the site of InsP$_3$ production.

An important question concerns the mechanism(s) responsible for this complex regulation of the InsP$_3$-gated channel. Our working hypothesis has been that the previously reported Ca-dependent decrease in InsP$_3$ binding is involved. Although micromolar Ca has been reported to completely inhibit InsP$_3$ binding to cerebellar membranes (Worley et al., 1987; Supattapone et al., 1988), our results reveal only a partial (<50%) inhibition of InsP$_3$ binding. As 95-99% of the InsP$_3$ receptors in the cerebellum have been shown to be of the type 1 isoform (Sudhof et al., 1991; Wojcikiewicz, 1995), it is unlikely that this partial inhibition is due to heterogeneity of InsP$_3$ receptors. Instead, the Ca-dependent decrease in InsP$_3$ binding appears to reflect a change in the affinity for InsP$_3$. This was first suggested in a report showing that the $K_d$ for InsP$_3$ binding to rat cerebellar membranes increased from 0.04 to 0.12 $\mu$M (Joseph et al., 1989). Such a shift in InsP$_3$ affinity has also been observed in aortic smooth muscle membranes (Benevolensky et al., 1994). Using binding conditions identical to those used for the channel activity determinations, the present study also shows a Ca-dependent shift in InsP$_3$ affinity, though the calculated $K_d$s are substantially higher than those previously reported. Thus, the binding affinities for InsP$_3$ reported in the present study are comparable to the calculated InsP$_3$ affinity for channel activation. The reason for the relatively high $K_d$ values in the present study involves in large part the high temperature dependence of the binding constant ($Q_{10} = 2.3$ for the cerebellar membranes). That is, InsP$_3$ binding studies are typically done on ice (0°C), whereas channel activity determinations are done at room temperature (23°C). In the present study, however, efforts were made to closely match both the InsP$_3$ binding and channel analyses. A similar $Q_{10}$ (2.0) has been reported for the $K_d$ of InsP$_3$ binding to basophilic leukemia cells (Watras et al., 1994), which was useful for modeling Ca release using InsP$_3$ binding data.

The eight-state model originally proposed for the regulation of the InsP$_3$-gated Ca channel (De Young and Keizer, 1992) represents one possible explanation for the bell-shaped Ca dependence of channel activity at low InsP$_3$ concentrations. Yet this eight-state model is unable to explain the relief of Ca-dependent inhibition of InsP$_3$-gated channel activity at high InsP$_3$ concentrations. We hypothesized that a low affinity InsP$_3$ binding site may be involved, and provided evidence for its existence using ligand binding assays. To fit the data at high InsP$_3$ concentrations, the eight-state model was therefore extended to include the 10 $\mu$M InsP$_3$ binding site, yielding a 16-state model (Kaftan et al., 1997).

In an effort to both explain the steady state channel data and extract kinetic information on InsP$_3$-gated Ca release, we used a novel approach that involves consideration of the channel as a unit. Previous models have focused on an individual InsP$_3$ receptor, predicting various states of the monomer, and then calculating probabilities of each combination of states in a tetrameric complex. The latter approach was used when extending the previously reported eight-state model of the InsP$_3$ receptor (De Young and Keizer, 1992) to 16 states (Kaftan et al., 1997), and we obtained reasonable fits of the channel data. A stochastic model has recently been proposed (Swillens et al., 1998), though it assumed only one InsP$_3$ binding site per channel complex, which is likely an oversimplification. The present model provides a more realistic representation of the channel with four medium-affinity InsP$_3$ binding sites per channel complex (Maeda et al., 1988; Supattapone et al., 1988).
and InsP3 binding data, it is important to ascertain the cytosolic region of the InsP3 receptor (Sienaert et al., 1992; Sienaert et al., 1996, 1997). The number of possible states of the channel could be greatly reduced, thereby allowing for the kinetic simulations of channel activity.

The mathematical model in the present study requires just four Ca binding sites per tetrameric channel complex. This is consistent with our initial observation (Bezprozvanny et al., 1991) that in the presence of 2 μM InsP3 the bell-shaped Ca dependence of channel activity could be fit assuming that two molecules of Ca were needed to open the channel, whereas two molecules of Ca appeared to close the channel. A similar stoichiometry of four divalent cation sites per channel complex was obtained when Mn was substituted for Ca (Striggow and Ehrlich, 1996). Examination of Ca binding to the cloned/expressed receptor fragments raises the possibility of up to eight Ca binding sites per InsP3 receptor monomer (Mignery et al., 1992; Sienaert et al., 1996, 1997). Seven of these Ca binding sites appear to reside on the cytosolic region of the InsP3 receptor (Sienaert et al., 1997), though the Ca affinity of only one of these sites (Kd 0.8 μM Ca, Hill coefficient 1.0) has been determined (Sienaert et al., 1996). The predicted Kd for Ca binding in the present study (0.7 μM, Table I) is consistent with the latter report. It has been hypothesized, based on the cation selectivity of the stimulation and inhibition of InsP3-induced Ca release (Marshall and Taylor, 1994; Sienaert et al., 1996; Striggow and Ehrlich, 1996), that Ca binding to at least three distinct cytosolic sites regulates InsP3-gated channel activity (Sienaert et al., 1997). For simplicity of the mathematical model, it is assumed that there are four distinct Ca binding sites on the channel, with Ca binding to one site altering the Ca affinity of the other sites in the channel complex. Inclusion of multiple Ca binding sites per InsP3 receptor monomer in the model is possible, and would be expected to increase the freedom in the model and provide even better fits of the channel and binding data, but at the cost of a considerably larger matrix calculation. As the identities of regulatory Ca binding sites become available, the mathematical model will be refined to more accurately represent the molecular details of channel structure.

Although the proposed model provides an accurate simulation of steady state InsP3-gated channel activity and InsP3 binding data, it is important to ascertain the physiological relevance of an InsP3 binding site with a dissociation constant of ~10 μM, particularly if the medium affinity InsP3 binding site has an affinity 30× lower (0.3 μM) at 22°C. It should be appreciated, however, that the medium affinity InsP3 binding site exhibited a strong temperature dependence (Q10 = 2.3), so that at 37°C, the dissociation constant of the medium affinity InsP3 binding site is predicted to approach 1 μM. The temperature dependence of the low affinity InsP3 binding site was difficult to measure, but it appeared to be relatively temperature independent. There are reports of ligand binding sites with low (or reversed) temperature dependence, where binding affinity is mainly entropy driven; it is not possible to accurately predict a priori if a given binding site will have a high or low temperature dependence of ligand binding (Testa et al., 1987). The low level of specificity of the low affinity site for 1,4,5-InsP3 versus 1,3,4,5-InsP4 (Kaftan et al., 1997) is in part consistent with the apparent low temperature dependence of this site. Thus, the difference in dissociation constants between the medium and low affinity InsP3 binding sites may be as low as 10-fold at the physiological temperature of 37°C (i.e., 1 vs. 10 μM).

At first glance, dissociation constants of 1–10 μM seem to be unexpectedly high, although review of the literature indicates that at physiological temperatures, rather high InsP3 concentrations may be needed to release Ca (Putney, 1990). In the case of cerebellar Purkinje cells, flash photolysis studies indicated the need for at least 9 μM intracellular InsP3 to induce Ca release, with Ca release increasing progressively as InsP3 concentration was elevated up to 80 μM (Khodakhah and Ogden, 1995). Moreover, it has been reported that sustained elevation of intracellular Ca can be observed using high concentrations (100 μM) of either InsP3 or the poorly hydrolyzed InsP3 analogue InsP5 (Wakui et al., 1989; Petersen et al., 1991). Furthermore, relatively high InsP3 concentrations have been noted in some cell types under basal (0.1–3 μM) and agonist-induced (1–20 μM) conditions (Putney, 1990). Thus, InsP3 dissociation constants of 1–10 μM at 37°C may be of physiological significance.

In summary, the present study provides a simple mathematical model of the cerebellar InsP3-gated channel, which provides an accurate simulation of InsP3-gated channel activity over a broad range of InsP3 and Ca concentrations. The model incorporates the well known “medium affinity” InsP3 binding site, and takes into account its temperature and Ca dependence. The model also includes a low affinity InsP3 binding site that exhibits little Ca or temperature dependence. Individual rate constants were incorporated into the model to allow kinetic simulations. It is expected that this novel model will provide a foundation for subsequent studies aimed at elucidating the molecular mechanisms underlying the complex behavior of the InsP3-gated channel.

847 M o r a r u e t a l.
Bootman, M.D., L. Missiaen, J.B. Parys, H. De Smedt, and R. Abdel-Latif. 1986. Calcium-mobilizing receptors, polyphosphoinositides, and the generation of second messengers. Pharmacol. Rev. 38:227–272.

Benevolensky, D., I. Moraru, and J. Watras. 1994. Micromolar calcium reduces the affinity of the inositol 1,4,5-trisphosphate receptor in smooth muscle. Biochem. J. 299:631–636.

Berridge, M.J., and R.F. Irvine. 1989. Inositol phosphates and cell signalling. Nature 341:197–205.

Bezprozvanny, I. 1994. Theoretical analysis of calcium wave propagation based on inositol (1,4,5)-trisphosphate (InsP3) receptor functional properties. Cell Calc. 16:151–166.

Bezprozvanny, I., J. Watras, and B.E. Ehrlich. 1991. Bell-shaped calcium-response curves of Ins(1,4,5)P3 and calcium-gated channels from endoplasmic reticulum of cerebellum. Nature 351:751–754.

Bootman, M.D., L. Missiaen, J.B. Parys, H. De Smedt, and R. Casteels. 1995. Control of inositol 1,4,5-trisphosphate-induced Ca2+ release by cytosolic Ca2+. Biochem. J. 306:445–451.

Bradford, M.M. 1976. A rapid and sensitive method for the quantification of microgram quantities of protein utilizing the principle of protein-dye binding. Anal. Biochem. 72:248–254.

Chadwick, C.C., A. Saito, and S. Fleischer. 1990. Isolation and characterization of the inositol trisphosphate receptor from smooth muscle. Proc. Natl. Acad. Sci. USA. 87:2132–2136.

Clapham, D.E. 1995. Calcium signaling. Cdl. 80:259–268.

Colquhoun, D., and A.G. Hawkes. 1983. The principles of the stochastic interpretation of ion-channel mechanisms. In Single Channel Recording. Plenum Publishing Corp., New York. 135–176.

De Young, G.W., and J. Keizer. 1992. A single-pool inositol 1,4,5-trisphosphate-receptor-based model for agonist-stimulated oscillations in Ca concentration. Proc. Natl. Acad. Sci. USA. 89:9895–9899.

Fabio, A. 1988. Computer programs for calculating total from specified free or free from specified total ionic concentrations in aqueous solutions containing multiple metals and ligands. Methods Enzymol. 157:378–417.

Finch, E.A., T.J. Turner, and S.M. Goldin. 1991. Calcium as a coagonist of inositol 1,4,5-trisphosphate-induced calcium release. Science 252:443–446.

Hannaert-Merah, Z., L. Combettes, J.-F. Coquill, S. Swillens, J.-P. Mauger, M. Clarot, and P. Chameil. 1995. Characterization of the co-agonist effects of strontium and calcium on myo-inositol trisphosphate-dependent ion fluxes in cerebellar microsomes. Cell Calc. 18:390–399.

Hille, B. 1992. Gating mechanisms. In Ionic Channels of Excitable Membranes. Sinauer Associates, Inc., Sunderland, MA. 472–504.

Horn, R. 1991. Estimating the number of channels in patch recordings. Biophys. J. 60:433–439.

Iino, M. 1990. Biphasic Ca2+ dependence of inositol 1,4,5-trisphosphate-induced Ca release in smooth muscle cells of the guinea pig taenia caeci. J. Gen. Physiol. 95:1103–1122.

Joseph, S.K., H.L. Rice, and J.R. Williamson. 1989. The effect of external calcium and pH on inositol trisphosphate-mediated calcium release from cerebellum microsomal fractions. Biochem. J. 258:261–265.

Kafata, E.J., B.E. Ehrlich, and J. Watras. 1997. Inositol 1,4,5-trisphosphate (InsP3) and calcium interact to increase the dynamic range of InsP3 receptor-dependent calcium signaling. J. Gen. Physiol. 110:529–538.

Khodakhah, K., and D. Ogden. 1995. Fast activation and inactivation of inositol trisphosphate-evoked Ca2+ release in rat cerebellar Purkinje neurones. J. Physiol. 487:343–358.

Maeda, N., M. Niinobe, K. Nakahira, and K. Mikoshi. 1988. Purification and characterization of P400 protein, a glycoprotein characteristic of Purkinje cell, from mouse cerebellum. J. Neurochem. 51:1724–1730.

Marshall, I., and C. Taylor. 1994. Two calcium binding sites mediate the interconversion of liver inositol 1,4,5-trisphosphate receptors between three conformational states. Biochem. J. 301:591–598.

Mignery, G.A., P.A. Johnston, and T.C. Sudhof. 1992. Mechanism of Ca2+ inhibition of inositol 1,4,5-trisphosphate (InsP3) binding to the cerebellar InsP3 receptor. J. Biol. Chem. 267:7450–7455.

Payne, R., T.M. Flores, and A. Fein. 1990. Feedback inhibition by calcium limits the release of calcium by inositol trisphosphate in Limulus ventral photoreceptors. Neuron. 4547–555.

Petersen, C.C.H., E.C. Toescu, B.V.L. Potter, and O.H. Petersen. 1991. Inositol trisphosphate produces different patterns of cytoplasmic Ca2+ spiking depending on its concentration. FEBS Lett. 293:179–182.

Putney, J. 1990. The integration of receptor-regulated intracellular calcium release and calcium entry across the plasma membrane. Curr. Top. Cell Regul. 31:111–127.

Sienaert, I., H. De Smedt, J.B. Parys, L. Missiaen, S. Vanlingen, H. Sipma, and R. Casteels. 1996. Characterization of a cytosolic and a luminal Ca2+ binding site in the type I inositol 1,4,5-trisphosphate receptor. J. Biol. Chem. 271:27005–27012.

Sienaert, I., L. Missiaen, H. De Smedt, J.B. Parys, H. Sipma, and R. Casteels. 1997. Molecular and functional evidence for multiple Ca2+-binding domains in the type 1 inositol 1,4,5-trisphosphate receptor. J. Biol. Chem. 272:25899–25906.

Striggow, F., and B.E. Ehrlich. 1996. The inositol 1,4,5-trisphosphate receptor of cerebellum. Mn2+ permeability and regulation by cytosolic Mn2+. J. Gen. Physiol. 108:115–124.

Sudhof, T.C., C.L. Newton, B.T. Archer III, Y.A. Ushkaryov, and G.A. Mignery. 1991. Structure of a novel InsP3 receptor. EMBO (Eur. Mol. Biol. Organ.) J. 10:3199–3206.

Supattapone, S., P.F. Worley, J.M. Baraban, and S.H. Snyder. 1988. Solubilization, purification, and characterization of an inositol trisphosphate receptor. J. Biol. Chem. 263:1530–1534.

Swillens, S., P. Chameil, L. Combettes, and G. Dupont. 1998. Stochastic simulation of a single inositol 1,4,5-trisphosphate-sensitive Ca2+ channel reveals repetitive openings during 'blip-like' Ca2+ transients. Cell Calc. 23:291–302.

Tang, Y., J.L. Stephenson, and H.G. Othmer. 1996. Simplification and analysis of models of calcium dynamics based on IP3-sensitive calcium channel kinetics. Biophys. J. 70:246–263.
Testa, B., P. Jenner, G.J. Kilpatrick, N. el Tayar, H. Van de Waterbeemd, and C.D. Marsden. 1987. Do thermodynamic studies provide information on both the binding to and the activation of dopaminergic and other receptors? Biochem. Pharmacol. 36:4041–4046.

Wakui, M., B.V.L. Potter, and O.H. Petersen. 1989. Pulsatile intracellular calcium release does not depend on fluctuations in inositol trisphosphate concentration. Nature 339:317–320.

Watras, J., I. Bezprozvanny, and B.E. Ehrlich. 1991. Inositol 1,4,5-trisphosphate-gated channels in cerebellum—presence of multiple conductance states. J. Neurosci. 11:3239–3245.

Watras, J., I. Moraru, D.J. Costa, and L.A. Kindman. 1994. Two inositol 1,4,5-trisphosphate binding sites in rat basophilic leukemia cells: relationship between receptor occupancy and calcium release. Biochemistry. 33:14359–14367.

Wojcikiewicz, R.J. 1995. Type I, II, and III inositol 1,4,5-trisphosphate receptors are unequally susceptible to down-regulation and are expressed in markedly different proportions in different cell types. J. Biol. Chem. 270:11678–11683.

Worley, P.F., J.M. Baraban, S. Supattapone, V.S. Wilson, and S.H. Snyder. 1987. Characterization of inositol trisphosphate receptor binding in brain. Regulation by pH and calcium. J. Biol. Chem. 262:12132–12136.