Generalized Inter-class Loss for Gait Recognition

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ABSTRACT

Gait recognition is a unique biometric technique that can be performed at a long distance non-cooperatively and has broad applications in public safety and intelligent traffic systems. Previous gait works focus more on minimizing the intra-class variance while ignoring the significance in constraining inter-class variance. To this end, we propose a generalized inter-class loss which resolves the inter-class variance from both sample-level feature distribution and class-level feature distribution. Instead of equal penalty strength on pair scores, the proposed loss optimizes sample-level inter-class feature distribution by dynamically adjusting the pairwise weight. Further, in class-level distribution, generalized inter-class loss adds a constraint on the uniformity of inter-class feature distribution, which forces the feature representations to approximate a hypersphere and keep maximal inter-class variance. In addition, the proposed method automatically adjusts the margin between classes which enables the inter-class feature distribution to be more flexible. The proposed method can be generalized to different gait recognition networks and achieves significant improvements. We conduct a series of experiments on CASIA-B and OUMVLP, and the experimental results show that the proposed loss can significantly improve the performance and achieves the state-of-the-art performances.

CCS CONCEPTS
• Computing methodologies → Biometrics; Supervised learning by classification; Neural networks.

KEYWORDS
Gait recognition, metric learning

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1 INTRODUCTION

Gait recognition is a biometric technique based on unique walking patterns of pedestrians. Compared to other biometrics such as face, fingerprint or iris, gait can be captured at a distance without the cooperation of subjects or intrusion to them. Therefore, it has been applied to many applications recently, such as crime prevention, forensic identification, public security, and intelligent traffic systems [8, 41, 52].

Compared to other image recognition tasks, gait recognition has the challenge of larger intra-class variance and smaller inter-class variance. The large intra-class variance is mainly due to the large visual dissimilarity among silhouettes from different angles and the same pedestrian wearing different clothes. The small inter-class variance is mainly caused by the following reason: although different pedestrians have different walking patterns, their gait silhouette frames are very similar because pedestrians have the same body structures (head, torso, arms and legs), similar body proportions, and similar walking postures including raising one leg, stepping forward, shifting weight from one leg to another, etc. Many effective works addressing intra-class variance problem have been proposed, such as cross-view gait recognition [57, 59, 64] and cross-cloth gait recognition [11, 35, 68], and achieve promising performances. However, most previous works overlook the importance of small inter-class variance and only address it implicitly.

Prior gait recognition works [5, 15, 19, 35, 46, 55] mainly focus on resolving intra-class variance by designing network architectures, while incidentally addressing the small inter-class variance by extracting fine-grained features from the designed networks. Previous approaches in gait recognition are categorized into two types: model-based [1, 26, 32] and appearance-based [5, 15, 19, 35, 46, 55]. The model-based methods use three-dimensional models and convey more information than two-dimensional ones, thus magnifying the inter-class variance. But model-based methods are highly
To address the small inter-class variance, explicitly constraining the inter-class feature distribution is beneficial. From sample-level perspective, some samples of the same viewpoint from different classes are close to each other due to visual similarity. They need to be emphasized to increase their distances and thus the inter-class variance increases. However, previous gait works [4, 5, 11, 21, 31, 35] usually treat pairs from different classes inflexibly, where the penalty strength on pair scores is restricted to be equal. From class-level perspective, constraining the inter-class feature distribution to be more uniform can increase inter-class variance. Previous works [27, 29, 30, 33, 34, 39, 59] seldom have constraints on inter-class distribution, resulting in lack of spatial symmetry, which is not optimal in keeping maximal mutual information. Nevertheless, margin aims to constrain the distance between classes, but prior works treat all pedestrians equally with the same given margin [4, 5, 11, 21], which lacks flexibility for optimization. Also, different classes with the same given margin lack ability to discriminate between each other.

To this end, we propose a generalized inter-class loss to resolve the inter-class variance problem from both sample-level and class-level. From sample-level perspective, the proposed generalized inter-class loss treats different pairs with dynamic and automatic coefficients, which enables different inter-class samples to dynamically adjust their distances from the anchor class.

Further, from class-level perspective, the proposed generalized inter-class loss adds a constraint on uniformity of inter-class feature representation and has advantages threefold. Firstly, uniformity prefers the inter-class feature distribution that preserves maximal information. The proposed similarity cross entropy (SimCE) in generalized inter-class loss can be regarded as a variation of von Mises-Fisher kernel density estimation [14, 16, 54], and forces the inter-class feature distribution to approximate a hypersphere in high dimension space. Thus, inter-class uniformity enables maximal inter-class variance. Secondly, the proposed loss is robust with respect to inter-class feature representation differences in its local area. Thirdly, to address the fixed given margin between different classes, the proposed generalized inter-class loss enables automatically adjusting margins between different classes and forces a flexible inter-class feature distribution.

Fig. 1 is the TSNE visualization of test features. It can be clearly seen that the feature distribution is more uniform, those hard exemplars are effectively optimized and the suboptimal representations in red boxes are decreasing.

The contributions of the proposed method are summarized as follows:

- We propose a unified method to resolve the inter-class variance of gait features from both sample-level and class-level, which dynamically and automatically adjusts the penalty strength on pair scores and margins between different classes.
- We further analyze the properties of the proposed method from three aspects, namely inter-class hard mining, uniformity and robustness of inter-class feature distribution, and dynamic margin. And we illustrate how these properties constrain a better inter-class feature distribution.
- The proposed gait recognition method improves the performance regardless of model structure. Experimental results on public datasets CASIA-B and OUMLP achieve state-of-the-art performances, especially with an improvement (6.2%) in different cloth (CL) condition.

2 RELATED WORKS
2.1 Gait Recognition

Gait recognition [5, 19, 31, 40, 43, 57] is to learn the unique spatio-temporal pattern about the human gait characteristics to obtain its identity information. The gait model input is bipartite: 3D based methods including Gait Energy Image (GEI)-based, set-based, and 3DCNN-based, extract fine-grained features which enlarge inter-class variance. But the above approaches do not explicitly constrain inter-class feature distribution.

To further improve the spatial temporal gait representation, Zhang et al. [65] utilizes a temporal attention mechanism and adaptively adjusts the weights of different frames. GaitNet [67, 68] and ICDNet [30] emphasize disentangled representation learning. GAN is also utilized [7, 60] to generate more data and help with feature constructing. SelfGait [39] uses self-supervised learning to perform gait recognition. Gait in the wild attracts researchers’ attention [63, 71], which focuses on real gait conditions and provides datasets in the wild. However, most of the works above focus more on addressing large intra-class variance and seldom consider small inter-class variance, which is of the same importance as well.
2.2 Metric Learning in Gait recognition
In gait recognition, the most popular loss includes triplet loss, CE classification loss, contrastive loss and hybrid loss. CE classification loss in gait recognition [1, 9, 10, 19, 45, 49, 56, 57, 60] is mainly utilized after prediction head, and takes low-dimensional classification logits as inputs to predict classification outputs. In recent years, triplet loss gains popularity in state-of-the-art gait recognition methods [4, 5, 11, 21, 27, 29–31, 33–35, 39, 59], which compares a baseline input (anchor) to a positive sample with the same identity, and a negative sample with a different identity. Triplet loss function aims to reduce the dissimilarity between feature vectors from the same subject and increase dissimilarity between feature vectors from different subjects. Gait recognition contrastive loss [28, 30, 62] is usually in the form of Fisher discriminant contrastive [6, 12]. If the samples are anchor and neighbor, they are pulled towards each other. Otherwise, their distance is increased. In other words, this contrastive loss performs like the triplet loss sequentially rather than simultaneously. Hybrid loss is often utilized as a combination of the loss discussed above. Other metrics adjust their loss functions corresponding to the network special modules. GaitNet [48] has a segmentation network and a recognition network, and designs the corresponding segmentation loss which is a sigmoid of square error of predicted segmentation mask and the ground truth, and a recognition loss which contains an id loss and a siamese loss. ICDNet [30] metric contains a triplet loss, a contrastive loss and a reconstruction loss which aims to reconstruct the disentangled part. In this paper, we focus more on analyzing the loss properties on inter-class variance in gait recognition task.

3 INTER-CLASS FEATURE DISTRIBUTION
3.1 Problem Formulation
We formulate the inter-class feature distribution loss problem in gait recognition as follows: given a objective function $\mathcal{L}$, and a fixed network architecture, after training to convergence, the loss stays stable, i.e. $\Delta L \leq \epsilon$, we denote the converged network parameters as $W(\mathcal{L})$. Then for every anchor feature $a$, we denote the positive sampled feature as $p$, and negative sampled feature as $n$, where the corresponding $a, p, n$ are computed by input silhouette sequences and $W(\mathcal{L})$. Since we focus on inter-class distribution, relative feature differences $u = a - p, v = a - n$ are more informative than a single feature. Thus we do a coordinate conversion. Then to find a inter-class feature distribution is to find a solution in Eq.1.

$$\min_{\mathcal{L}} \mathcal{L}_{eval}(a, u, v, W(\mathcal{L}))$$

(1)

Usually the loss $\mathcal{L}$ on evaluation/test dataset is the same as on train dataset $\mathcal{L}$, and in the following context we do not differentiate the two of them. An ideal objective $\mathcal{L}$ generalizes well and is small on both train set and test set. Note that it is small but not zero because the dataset inevitably contains noise.

In this paper, we explore how a loss interacts with inter-class feature distribution in gait recognition task, and we carefully analyze the properties of objectives in gait recognition from three aspects: explicit inter-class hard mining, uniformity and robustness of inter-class distribution, and dynamic margin.

3.2 Explicit Inter-class Hard Mining
According to Eq.1, we firstly analyze the first order gradient of $\mathcal{L}$ on $v$, which actually indicates hard relations mining. The first order gradient on $v$ affects the sample-wise inter-class feature distribution: gradient on $v$ is to push it with penalizing strength to be further from anchor point, and pushing the smaller $v$ stretches the hard classes to discriminate from each other and increases inter-class variance. Recent gait recognition works utilizes vanilla triplet loss [4, 5, 11, 21, 27, 29–31, 33–35, 39, 59] as a prevailing objective (Eq.2), which equally treats all triplets and ignores the importance of mining hard relations. FaceNet [44] addresses this by selecting the hardest negative exemplars within a batch. However, this solution brings two doubts. Firstly, as Hermans et al. [18] state, selecting all positives is more stable compared to selecting the hardest positives. And we analyze the possible reason is the lack of triplets selected: hardest-only principle significantly reduces the number of triplets and increases the possibility to overfit out-of-distribution exemplars, which are prevalent in gait dataset because of preprocessing. Secondly, to obtain a meaningful representation of the distances, FaceNet [44] samples numerous faces per identity $^1$, which is impractical in gait recognition because of the dataset size.$^2$. Despite the large batch size, selecting the hardest negatives can in practice lead to bad local minima early in training, specifically, it results in a collapsed model. Thus, instead of selecting the hardest exemplars, it is straightforward to weight each anchor-positive and anchor-negative pair, i.e., to down-weight the loss assigned to well-classified pairs.

$$\mathcal{L}_{tri} = \text{ReLU}(m + \text{dist}(u) - \text{dist}(v))$$

(2)

where $m$ is the margin. In gait recognition task, $\text{dist}(\cdot)$ is usually Euclidean distance $\|\cdot\|_2$.

To assign different weights automatically to different triplets, we adopt similarity matrix $S$ as in Eq.3 for the following reasons. Firstly, inspired by focal loss [36] which utilizes a function of the input of the loss to re-weight every loss term, the similarity matrix can also be computed online from the input of triplet loss and requires no additional modules or alternating the network structure, which is simple and can be easily generalized. Secondly, similarity matrix, although simple in its form, is a good reflection of pair distance, and the normalized form of similarity matrix $S/S_{max}$ is informative for pair comparison in a batch. We mine hard relations from a granularity of pairs, instead of triplets or batches, which is more flexible and detailed.

$$\mathcal{L}_{s-tri} = \text{ReLU}(m + w_{a,p}\text{dist}(a, p) - w_{a,n}\text{dist}(a, n))$$

$$= \text{ReLU}(m + f(S_{a,p})\text{dist}(a, p) - f(S_{a,n})\text{dist}(a, n))$$

(3)

where the $w_{a,p}$, $w_{a,n}$ are the re-weighting terms, and $S_{a,p}$, $S_{a,n}$ are the corresponding entries in the similarity matrix, and $f(\cdot)$ here is a function inversely proportional to $S$. We adopt a linear $f(x) = (1 - x)/2$. More carefully designed form of $f(\cdot)$ is sure to further improve the performance, but it is not the priority of this paper.

Since $f(\cdot)$ is a function inversely proportional to $S$, it can automatically mine hard triplet pairs. If the anchor-positive pair are well-classified, $S_{a,p}$ is rather big, $w_{a,p}$ is thus small, and this term

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1. In FaceNet [44], batch size is 1800.
2. In gait recognition, batch size is usually 64 or 128.
well-clustered spherical spaces are linearly separable, while this different color denotes different walking conditions. And LMCL [53] introduces a cosine and a margin to classification loss variance. Uniformity prefers a feature distribution that preserves since the id-relevant information is not totally disentangled with id-
by center feature results in destruction of the intra-class structure. And the network inevitably keeps identity, there is an intra-class structure since the sequences of the in face recognition. However, when combined with gait recognition, in image classification on CIFAR, and Large Margin Cosine Loss cosine loss (CoCo Loss) [38] introduces cosine loss to center loss feature representation to be more uniform, such as congenerous uniformly distributed in the feature space (Fig.1(a)).

Prior gait recognition lacks constraints on inter-class features to be distribution to approach a hypersphere and increase separability. Thus, the intra-class structure throws features extracted from front convolution layers away as well as ignoring the valuable information in these features. Thus, we propose to keep the intra-class structure without using class centers, and propose the cross entropy of similarity matrix between features representations (SimCE loss) as in Eq.4. We will carefully analyze why this SimCE loss helps with inter-class variance.

\[ \mathcal{L}_{\text{SimCE}}(a, u, v) = -\log \frac{e^{a(u-a)/T}}{e^{a(u-a)/T} + e^{a(a-v)/T}} \quad (4) \]

**Hypersphere Embedding.** A mixture of von Mises-Fisher kernel density estimations (Eq.5) constructs a hypersphere embedding. And the form \( \frac{\exp \gamma x}{\gamma^\nu I_\nu(\gamma)} \) can be explained by a von Mises-Fisher Mixture Model (vMFMM) [14, 16, 54]. Training with \( \mathcal{L}_{\text{SimCE}} \) minimizes every \( \kappa \) and \( \nu \) in vMF function determine uniformity of random variables distribution on a sphere. The smaller the \( \kappa \) is, the more uniform the distribution is. Note that we generalize the \( \mu \) from \( ||\mu||_2 = 1 \) to \( \mu \) in Euclidean space. Thus, beyond the triplet loss which utilizes Euclidean constraints in high dimension space, adding SimCE loss provides an additional constraint that forces the features to be more similar to uniform hypersphere embeddings.

\[ \mathcal{V}_d(x|\mu, \kappa) = C_d(\kappa) \exp(\kappa \mu^T x) \quad (5) \]

where, \( \mu \) denotes the mean and \( \kappa \) denotes the concentration parameter (with \( \kappa \geq 0 \)). \( C_d(\kappa) = \frac{\kappa^{d/2-1}}{(2\pi)^{d/2} \Gamma(d/2)} \) is the normalization constant, where \( I_\nu(\cdot) \) is the modified Bessel function of the first kind. The shape of the vMF distribution depends on the value of the concentration parameter \( \kappa \).

Euclidean triplet loss forces the features to have radius disparity and is radius discriminative, while SimCE loss forces the features to have tangential disparity, and is tangential separable. Thus these two losses together results in a more uniformly distributed feature space, as in Fig.1(b).

**3.3 Uniformity and Robustness of Inter-class Distribution**

**3.3.1 Uniformity and Hypersphere.** Improving uniformity of inter-class feature distribution is beneficial for increasing inter-class variance. Uniformity prefers a feature distribution that preserves maximal information. In addition, Wang et al. [54] points out that well-clustered spherical spaces are linearly separable, while this does not hold for Euclidean spaces. Thus we expect the feature distribution to approach a hypersphere and increase separability. Prior gait recognition lacks constraints on inter-class features to be uniformly distributed in the feature space (Fig.1(a)).

Previous works utilizes similarity in cosine form to constrain the feature representation to be more uniform, such as congenerous cosine loss (CoCo Loss) [38] introduces cosine loss to center loss in image classification on CIFAR, and Large Margin Cosine Loss (LMCL) [53] introduces a cosine and a margin to classification loss in face recognition. However, when combined with gait recognition, CoCo Loss and LMCL utilize center class as the “ground truth” and force every feature to be close to the center, which is inferior for the following reason. As shown in Fig.2, in every gait class of one identity, there is an intra-class structure since the sequences of the same view and the same walking conditions are visually similar and stay close to each other. And the network inevitably keeps features extracted from front convolution layers and preserves visual similarity information. Simply approximating every feature by center feature results in destruction of the intra-class structure. Since the id-relevant information is not totally disentangled with id-irrelevant information (e.g., views, walking conditions), destruction of the intra-class structure throws features extracted from front convolution layers away as well as ignoring the valuable information in these features. Thus, we propose to keep the intra-class structure without using class centers, and propose the cross entropy of similarity matrix between features representations (SimCE loss) as in Eq.4. We will carefully analyze why this SimCE loss helps with inter-class variance.

**3.3.2 Robustness on Local Area.** Following the function Eq.1, we further analyze the property of second order gradient on \( v \) with a fixed \( a \), which indicates the robustness of the objective. And the objective function expectation on local area becomes:

\[ E_{\delta \sim \mathcal{U}[-\epsilon, \epsilon]} \mathcal{L}(a, u, v + \delta) \]

\[ \approx E_{\delta \sim \mathcal{U}[-\epsilon, \epsilon]} \left[ \mathcal{L}(a, u, v) + \delta \nabla_v \mathcal{L}(a, u, v) + 1/2 \delta^2 \nabla_v^2 \mathcal{L}(a, u, v) \delta \right] \quad (6) \]

where the second term in Eq.6 is canceled out since \( E[\delta] = 0 \) and the off-diagonal elements of the third term becomes 0 after taking the expectation on \( \delta \).

If Hessian is stable in a local region of \( L(a, u, v) \), then the quantity of Eq.6 can approximately bound the performance drop when suffering perturbation of unavoidable data noise or evaluation on test dataset, which improves robustness. As shown in Eq.8, the trace of the Hessian of the proposed \( \mathcal{L}_{\text{SimCE}} \) is bounded within 1, while in Eq.7, the trace of Hessian has no such bound in range of \([0, +\infty)\). The analysis indicates that triplet loss \( \mathcal{L}_{\text{tril}}(a, u, v) \) has less
robustness compared to the proposed \( L_{SimCE}(a, u, v) \).

\[
\text{trace}(H_{ij}(L_{tri})) = \sum_i \frac{||z_2 - (a_j) + \cos(\theta) \cdot ||v||_2}{||v||_2^2} \approx (n - 1) \cdot \frac{1}{||v||_2^2} \quad (7)
\]

\[
\text{trace}(H_{ij}(L_{SimCE})) = \sum_i \frac{e^a(a-u) + e^a(a-v)}{e^a(a-u) + e^a(a-v)} \leq 1/2 \quad (8)
\]

3.4 Dynamic Margin

Margin also depicts a property of the inter-class distribution and aims to constrain the distance between classes. Popular losses in gait recognition and face recognition (e.g., triplet loss [18], LMCL [53]) require a given fixed margin, which brings three doubts: semantic interpretability, training efficiency and noise overfitting. As in Eq.9, the SimCE term can be approximately represented as triplet loss with a dynamic margin \((an - ap)^2/T + 2T\), and is able to alleviate the above problems.

\[
L_{SimCE} = -\log \frac{e^{ap/T}}{e^{ap/T} + e^{an/T}} = \log(1 + \exp((an - ap)/T)) \approx \exp((an - ap)/T)
\]

\[
= 1 + (an - ap)/T + (an - ap)^2/2T^2 \quad (9)
\]

\[
= 1 - 1/2T(||a - n||^2 - ||a - p||^2 - (an - ap)^2/T)
\]

\[
\propto -(||a - n||^2 - ||a - p||^2 - (an - ap)^2/T)\]

Firstly, pushing all classes with the same given margin is not semantic interpretable. For example, class ‘001’ and class ‘002’ are all young females with similar body shapes and walking habits, while ‘003’ is a child and is dissimilar to ‘001’. If ‘001’ is the anchor, and the same given margin pushes ‘002’ and ‘003’ with the same distance \(m\), which lacks semantic interpretability. SimCE loss computes the similarity of feature pairs, and adaptively adjusts the distances between different classes. The larger the differences between \(ap\) and \(an\), the larger the dynamic margin \((an - ap)^2/T + 2T\) is. Thus, the inter-class feature distribution is further optimized.

Secondly, it is also inefficient for training since ‘002’ and ‘003’ are at the same margin \(m\) from ‘001’, and it requires further training to separate ‘002’ and ‘003’. In addition, if batch-hard triplet loss is utilized, it requires computational cost to generate a hard triplet. If the batch size is \([N, K]\), then following the work of hard triplet loss [18], it needs to compute \((N - 1) \times K\) pairs to output the hard triplet pairs. SimCE alleviates this by making use of all triplets and separating them with adaptive discriminative distances.

Finally, when the distance of anchor-positive and anchor-negative triplet satisfies the margin, this triplet is not taken into consideration when computing the final loss. Denote the number of nonzero triplets as \(N_{non}\). In gait recognition, we observe that \(N_{non}\) swiftly decays to a small integer, as in Fig.4, which indicates overfitting. After the early training period the structure of the class cluster is that the clean feature (circles) are the closest to the class center, and difficult dissimilar features (triangles) are far from the class center. After the network learns gradually, clean samples’ contribution to loss is zero, then the network continues to optimize other samples. As the noisy samples gradually reach a higher proportion, the discriminative boundaries in feature space get complicated and overfit noise. Moreover, by using a hard given margin, knowledge learned in the early training period is down-weighted. By adding the proposed loss, all features regardless of their distance from others are taken into consideration. At the same time, SimCE also mine hard pairs explicitly, which indicates that the hard exemplars are given with large loss. The proposed method alleviates the problem of noise making up a large proportion in the late training period.

To conclude, the proposed method optimizes inter-class distribution for the following reasons: 1) the proposed method has the property to force hypersphere embeddings in feature space with both Euclidean and angular constraints. 2) the proposed method provides a bounded Hessian in a local region of test accuracy and ensures the robustness of loss metric. 3) SimCE loss helps alleviate the degeneration caused by the fixed margin, improves semantic interpretability, training efficiency and alleviates noise overfitting.

3.5 From Three Terms to Multiple Terms

Inspired by contrastive loss [23], InfoNCE loss [51] and N-pair loss [47], which have similar forms to SimCE, we change SimCE with three terms to multiple terms because we aim to utilize multiple negative exemplars for constructing contrastive groups and for feature learning. Thus, m-SimCE every time considers \([N \times K]\) samples of \(N\) classes, where \(Batchsize = [N, K]\).\(^5\) The advantages and disadvantages of multiple terms are as follows.

\[
L_{m-SimCE} = -\log \frac{e^{ap/T}}{e^{ap/T} + e^{an/T} \times [K]} \quad (10)
\]

**Advantages.** Utilizing SimCE and triplet loss is actually equivalent to a two-class classification. Similar to the work of Zhang et al. [66], there is a need to enable the joint optimization of multiple instances within per-query optimization for gait recognition. As illustrated in

\(^5\)N refers to the number of classes, and K refers to the number of sequences sampled from every class.
We conduct our experiments on two commonly used public datasets CASIA-B and OUMVLP. CASIA-B. The CASIA-B dataset [70] is the popular cross-cloth gait database. It includes 124 subjects, each of which has 10 groups of videos. Among these groups, six of them are sampled in normal walking (NM), two groups are in walking with a bag (BG), and the rest are in walking in different cloth (CL). Each group contains 11 gait sequences from different angles (0°-180° and the sampling interval is 15°). Therefore, there are 124 (subject) × 10 (groups) × 11 (view angle) = 13,640 gait sequences in CASIA-B. The gait sequences of each subject are divided into train set and test set. Following the setting of previous works [5], in small-sample training (ST) the first 24 subjects (labeled in 001-024) are used for training and the rest 100 subjects are left for testing. In medium-sample training (MT), the first 62 subjects are used for training and the rest 62 subjects are left for test. In large-sample training (LT), the first 74 subjects are used for training and the rest 50 subjects are leaved for test. In the test stage, the sequences NM#01-NM#04 are taken as the gallery set, while the sequences NM#05-NM#06, BG#01-BG#02, and CL#01-CL#02 are considered as the probe set to evaluate the performance.

OUMVLP. The OUMVLP [50] dataset is one of the largest gait recognition open source databases, which contains 10,307 subjects in total. Each subject contains two groups of videos, Seq#00 and Seq#01. Each group of sequences is captured from 14 angles (0°-90°, 180°-270° and the sampling interval is 15°). Following the setting of previous works [5], We adopt the same protocol, i.e., 5,153 subjects are taken as training data and 5,154 subjects are used as test data to evaluate the performance of the proposed method. In the test stage, the sequences in Seq#01 are taken as the gallery set, while the sequences in Seq#00 are regarded as the probe set for evaluation.

4 EXPERIMENTS

4.1 Datasets

We conduct our experiments on two commonly used public datasets CASIA-B and OUMVLP.

CASIA-B. The CASIA-B dataset [70] is the popular cross-cloth gait database. It includes 124 subjects, each of which has 10 groups of videos. Among these groups, six of them are sampled in normal walking (NM), two groups are in walking with a bag (BG), and the rest are in walking in different cloth (CL). Each group contains 11 gait sequences from different angles (0°-180° and the sampling interval is 15°). Therefore, there are 124 (subject) × 10 (groups) × 11 (view angle) = 13,640 gait sequences in CASIA-B. The gait sequences of each subject are divided into train set and test set. Following the setting of previous works [5], in small-sample training (ST) the first 24 subjects (labeled in 001-024) are used for training and the rest 100 subjects are left for testing. In medium-sample training (MT), the first 62 subjects are used for training and the rest 62 subjects are left for test. In large-sample training (LT), the first 74 subjects are used for training and the rest 50 subjects are leaved for test. In the test stage, the sequences NM#01-NM#04 are taken as the gallery set, while the sequences NM#05-NM#06, BG#01-BG#02, and CL#01-CL#02 are considered as the probe set to evaluate the performance.

Figure 4: Loss tendency from iteration 0 to iteration 80k. Y-axis indicates the none-zero numbers of triplets in a batch. (a) baseline. (b) the proposed method.

Fig.3, more negative terms bring advantages including robustness to noise and a larger range for optimization. By enlarging the number of samples for every loss term, the influence of noise contributes less to the total loss. And as in Fig.3(a), the optimization direction is determined by two terms and is probable to be only optimal for this pair, while in Fig.3(b) optimization direction is more optimized.

Disadvantages. However, m-SimCE highly depends on intrinsic visual similarity to separate dissimilar features from similar ones. If the intrinsic similarity is large intra-class, the intra-class variance gets larger. In other words, the multiple term loss increases inter-class and intra-class variance simultaneously, and if the intra-class variance of datasets is large, m-SimCE harms the overall classification.

Guideline. Considering the advantages and disadvantages above, the guideline is that if the cross cloth condition makes up a high proportion in the dataset, we recommend using \( L_m \), and otherwise using \( L_s \). Or you can use a hyperparameter to adjust the weight of \( L_m \) and \( L_s \), which is not the prior of this paper.

Thus, we have two final generalized similarity loss form, combining similarity-triplet loss, cross entropy loss and SimCE loss (or multiple SimCE loss), as in Eq.11

\[
L_s = L_s-tri + L_{CE} + L_{SimCE}
\]

\[
L_m = L_s-tri + L_{CE} + L_m-SimCE
\]

(11)

4.2 Implementation Details

The baseline network is GaitGL [35], which utilizes global and local convolutional layers to extract global and local features, and uses local temporal aggregation to process the temporal information. We adopt the same preprocessing approach as [4] to obtain gait silhouettes for CASIA-B and OUMVLP. The loss function coefficients are all set to 1 in our experiments. We adopt the SGD optimizer [42] with 0.1 learning rate. The momentum and weight decay are set to 0.9 and 5e-4, respectively. The learning rate decays from 0.1 to 1e-4 with a cosine scheduler. We implement our method on the basis of OpenGait4.

CASIA-B In the setting of CASIA-B experiments, the iteration number is set to 80K. In each batch, the number of subjects and the number of sequences for each subject are set to (8, 8) and the input resolution is (64, 44). For evaluation, all silhouettes of gait sequences are used to obtain the final representation. In the CASIA-B ST, MT and LT settings, the iteration number is set to 60K, 80K and 80K, respectively.

OUMVLP In the setting of OUMVLP experiments, the iteration number is set to 210K. The number of subjects and the number of sequences for each subject are set to (32, 8) and the input resolution is (64, 44). For evaluation, all silhouettes of gait sequences are taken to obtain the final representation.

4.3 Results

4.3.1 Comparison with State-of-the-art Methods. CASIA-B. We compare our approach with state-of-the-art gait recognition approaches, including ViDP [20], CMCC [25], GaitSet [4], AE [61], MGAN [17], CNN-LB, CNN-3D, CNN-Ensemble [57], ACL [65],

https://github.com/ShiqiYu/OpenGait.git

Figure 5: Visualization of Similarity Matrix. The matrix size is 64’64, and batch size is [8,8]. (a) similarity matrix at iteration 1k. (b) similarity matrix at iteration 40k. (c) similarity matrix at iteration 80k.

Guideline. Considering the advantages and disadvantages above, the guideline is that if the cross cloth condition makes up a high proportion in the dataset, we recommend using \( L_m \), and otherwise using \( L_s \). Or you can use a hyperparameter to adjust the weight of \( L_m \) and \( L_s \), which is not the prior of this paper.

Thus, we have two final generalized similarity loss form, combining similarity-triplet loss, cross entropy loss and SimCE loss (or multiple SimCE loss), as in Eq.11

\[
L_s = L_s-tri + L_{CE} + L_{SimCE}
\]

\[
L_m = L_s-tri + L_{CE} + L_m-SimCE
\]

(11)
Table 1: Rank-1 accuracy (%) on CASIA-B under all view angles, different settings and conditions, excluding identical-view case. Bold and Italic fonts indicate the best and second-best results respectively.

| Probe                  | 0°  | 18° | 36° | 54° | 72° | 90° | 108° | 126° | 144° | 162° | 180° | Mean |
|------------------------|-----|-----|-----|-----|-----|-----|------|------|------|------|------|------|
| NM#5-6                 |     |     |     |     |     |     |      |      |      |      |      |      |
| ST(24)                 |     |     |     |     |     |     |      |      |      |      |      |      |
| GaitSet                | 53  | 45  | 42  | 35  | 32  | 28  | 25   | 28   | 32   | 38   | 42   | 36   |
| GaitGL (baseline)      | 51  | 49  | 45  | 41  | 37  | 34  | 31   | 34   | 37   | 41   | 45   | 40   |
| Ours ($L_m$)           | 52  | 47  | 45  | 41  | 37  | 34  | 31   | 34   | 37   | 41   | 45   | 40   |
| Ours ($L_s$)           | 50  | 46  | 43  | 39  | 35  | 32  | 29   | 32   | 35   | 39   | 43   | 38   |
| BG#1-2                 |     |     |     |     |     |     |      |      |      |      |      |      |
| GaitSet                | 54  | 47  | 43  | 39  | 35  | 32  | 29   | 32   | 35   | 39   | 43   | 38   |
| GaitGL (baseline)      | 49  | 44  | 40  | 36  | 33  | 30  | 27   | 30   | 33   | 36   | 40   | 35   |
| Ours ($L_m$)           | 50  | 46  | 43  | 39  | 35  | 32  | 29   | 32   | 35   | 39   | 43   | 38   |
| Ours ($L_s$)           | 49  | 45  | 42  | 38  | 35  | 32  | 29   | 32   | 35   | 39   | 43   | 38   |
| NM#5-6                 |     |     |     |     |     |     |      |      |      |      |      |      |
| CL#1-2                 |     |     |     |     |     |     |      |      |      |      |      |      |
| GaitSet                | 51  | 45  | 42  | 37  | 33  | 30  | 27   | 29   | 32   | 35   | 39   | 34   |
| GaitGL (baseline)      | 46  | 42  | 38  | 34  | 30  | 27  | 24   | 27   | 30   | 34   | 38   | 33   |
| Ours ($L_m$)           | 49  | 44  | 40  | 36  | 32  | 29  | 26   | 29   | 32   | 36   | 40   | 35   |
| Ours ($L_s$)           | 47  | 43  | 39  | 35  | 31  | 28  | 25   | 28   | 31   | 35   | 39   | 34   |
| MT(62)                 |     |     |     |     |     |     |      |      |      |      |      |      |
| BG#1-2                 |     |     |     |     |     |     |      |      |      |      |      |      |
| GaitSet                | 52  | 46  | 43  | 39  | 35  | 32  | 29   | 32   | 35   | 39   | 43   | 38   |
| GaitGL (baseline)      | 47  | 42  | 38  | 34  | 30  | 27  | 24   | 27   | 30   | 34   | 38   | 33   |
| Ours ($L_m$)           | 49  | 45  | 41  | 37  | 33  | 30  | 27   | 29   | 32   | 35   | 39   | 34   |
| Ours ($L_s$)           | 47  | 43  | 39  | 35  | 31  | 28  | 25   | 28   | 31   | 35   | 39   | 34   |
| CL#1-2                 |     |     |     |     |     |     |      |      |      |      |      |      |
| GaitSet                | 50  | 44  | 41  | 37  | 33  | 30  | 27   | 29   | 32   | 35   | 39   | 34   |
| GaitGL (baseline)      | 45  | 41  | 37  | 33  | 29  | 26  | 23   | 26   | 29   | 33   | 37   | 32   |
| Ours ($L_m$)           | 48  | 44  | 40  | 36  | 32  | 29  | 26   | 29   | 32   | 36   | 40   | 35   |
| Ours ($L_s$)           | 46  | 42  | 38  | 34  | 30  | 27  | 24   | 27   | 30   | 34   | 38   | 33   |
| LT(74)                 |     |     |     |     |     |     |      |      |      |      |      |      |
| BG#1-2                 |     |     |     |     |     |     |      |      |      |      |      |      |
| GaitSet                | 51  | 45  | 42  | 37  | 33  | 30  | 27   | 29   | 32   | 35   | 39   | 34   |
| GaitGL (baseline)      | 46  | 42  | 38  | 34  | 30  | 27  | 24   | 27   | 30   | 34   | 38   | 33   |
| Ours ($L_m$)           | 49  | 45  | 41  | 37  | 33  | 30  | 27   | 29   | 32   | 35   | 39   | 34   |
| Ours ($L_s$)           | 47  | 43  | 39  | 35  | 31  | 28  | 25   | 28   | 31   | 35   | 39   | 34   |

GaitPart [11] and GaitGL [35] on CASIA-B. The experimental results are shown in Table 1, and we summarize the results as follows: 1) the proposed approach achieves the best mean recognition accuracy and at nearly all view metrics. Both $L_s$ and $L_m$ improve the baseline by a large margin. The experiment results demonstrate the effectiveness of the proposed method. 2) we find that $L_s$ performs better on NM and BG conditions while $L_m$ surpasses other methods with a great performance margin in CL scenario. The reason can refer to Sec.3.5, the rise in CL is due to the advantages of generalized $L_m$, where it considers more terms to find a better optimization direction, while its inferior in NM is mainly due to the disadvantages in Sec.3.5. And our guideline is that if the CL makes up a high proportion in the dataset, we recommend using $L_m$, and otherwise using $L_s$. 3) in LT setting CL condition,
As shown in Tab.4, we conduct ex-
periments on OpenGait baseline, GaitSet [4], GaitGL [35], and the
results show that the proposed metric can improve the performances
of the baseline at all metrics consistently, regardless of baseline
backbones or network structures. The model agnostic property
further verifies that the proposed loss outperforms other popular
losses in gait recognition.

The ablation result is illustrated in Tab.3.
Note that the data augmentation is firstly sampled from many data
augmentation methods, and then is fixed (in experiments they are
random erase and image dilate) for all experiments from #2 to #5 for
the reason for this is illustrated in Sec.3.5. (4) Overall, the mean
accuracy rises by about 2%, which demonstrates the effectiveness
of the proposed methods.

## 5 CONCLUSION
In this work, we propose a generalized similarity loss to resolve the
small inter-class variance problem in gait recognition. We analyze
the properties of the proposed method from three aspects, namely
inter-class hard mining, uniformity and robustness of inter-class
feature distribution, and dynamic margin, and how these aspects
help with inter-class feature distribution. Extensive experiments
on CASIA-B and OUMVLP demonstrate that the proposed loss
achieves state-of-the-art performance greatly regardless of network
architecture in gait recognition.

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Multimedia*. 

### Table 2: Rank-1 accuracy (%) on OUMVLP under 14 probe views excluding identical-view cases.

| Method       | 0°  | 15° | 30° | 45° | 60° | 75° | 90° | 180° | 210° | 225° | 240° | 255° | 270° | Mean |
|--------------|-----|-----|-----|-----|-----|-----|-----|------|------|------|------|------|------|------|
| GEINet       | 23.2| 38.1| 48.0| 51.8| 47.5| 48.1| 43.8| 27.3 | 37.9 | 46.8 | 49.9 | 45.9 | 45.7 | 41.0 | 42.5 |
| GaitSet      | 79.3| 87.9| 90.0| 90.1| 88.0| 88.7| 87.7| 81.8 | 86.5 | 89.0| 89.2 | 87.2 | 87.6 | 86.2 | 87.1 |
| GaitPart     | 82.6| 88.9| 90.8| 91.0| 89.7| 89.9| 89.5| 85.2 | 88.1 | 90.0| 90.1 | 89.0 | 89.1 | 88.2 | 88.7 |
| GLN         | 83.8| 90.0| 91.0| 91.2| 90.3| 90.0| 89.4| 85.3 | 89.1 | 90.5| 90.6 | 89.6 | 89.3 | 88.5 | 89.2 |
| GaitGL(baseline) | 84.9| 90.2| 91.1| 91.5| 91.1| 90.8| 90.3| 88.5 | 88.6 | 90.3| 90.4 | 89.6 | 89.5 | 88.9 | 89.7 |
| Ours       | 87.1| 91.0| 91.4| 91.7| 91.5| 91.3| 91.0| 90.1 | 89.8| 90.6| 90.7 | 90.3 | 90.2 | 89.8 | 90.5 |

### Table 3: Component-wise analysis. Ablation study on CASIA-B, excluding identical-view cases.

| Method | Augmentation | s-triplet | SimCE | m-SimCE |
|--------|--------------|-----------|-------|---------|
| #1     |              |           |       |         |
| #2     | ✓            |           |       |         |
| #3     | ✓            | ✓         |       |         |
| #4     | ✓            | ✓         | ✓     |         |
| #5     | ✓            | ✓         | ✓     | ✓       |

### Table 4: Model agnostic results on CASIA-B dataset, excluding identical-view cases.

| Methods | NM  | BG  | CL  | Mean  |
|---------|-----|-----|-----|-------|
| OpenGait | 96.3| 92.2| 77.6| 88.7  |
| +Ours (L₈) | 97.9| 93.2| 78.7| 90.0  |
| GaitSet [5] | 95.8| 90.0| 75.4| 87.0  |
| +Ours (L₈) | 97.0| 92.6| 76.6| 88.7  |
| GaitGL [35] | 97.4| 94.5| 83.6| 91.8  |
| +Ours (L₈) | 97.6| 95.5| 87.2| 93.4  |

4.3.2 Model Agnostic Results. As shown in Tab.4, we conduct ex-
periments on OpenGait baseline, GaitSet [4], GaitGL [35], and the
results show that the proposed metric can improve the performances
of the baseline at all metrics consistently, regardless of baseline
backbones or network structures. The model agnostic property
further verifies that the proposed loss outperforms other popular
losses in gait recognition.

4.3.3 Ablation Study. The ablation result is illustrated in Tab.3.
Note that the data augmentation is firstly sampled from many data
augmentation methods, and then is fixed (in experiments they are
random erase and image dilate) for all experiments from #2 to #5 for
the reason for this is illustrated in Sec.3.5. (4) Overall, the mean
accuracy rises by about 2%, which demonstrates the effectiveness
of the proposed methods.

In this work, we propose a generalized similarity loss to resolve the
small inter-class variance problem in gait recognition. We analyze
the properties of the proposed method from three aspects, namely
inter-class hard mining, uniformity and robustness of inter-class
feature distribution, and dynamic margin, and how these aspects
help with inter-class feature distribution. Extensive experiments
on CASIA-B and OUMVLP demonstrate that the proposed loss
achieves state-of-the-art performance greatly regardless of network
architecture in gait recognition.

the proposed method on CL condition reaches 89.8%, which is a
significant performance, and the gap between NM and CL condition
decreases from 13.8% to 6.6%, which indicates that although large
appearance changes bring big data variations, CL variation can be
alleviated by loss design. 4) as illustrated in Fig.5, the similarity
matrix between a batch [8, 8] in 1k iteration, 40k iteration and
80k iteration, the 8 diagonal 8 * 8 blocks indicates the intra-class
similarity, and the 56 off-diagonal blocks indicate the inter-class
similarity. The similarity matrix at iteration 1k is close to randomly
distributed features, and after 40k iteration training, the similarity
intra-class increases and the diagonal blocks get closer to 1, and
after more iterations training, the inter-class similarity decreases
so that the off-diagonal blocks get closer to 0, indicating that the
feature representations are discriminative. 5) as shown in Fig.4(b),
the triplet loss number N_non of proposed generalized similarity loss
is larger than baseline, which indicates the overfitting is alleviated.
Therefore, the proposed method exploits a better metric in gait
recognition compared with SOTA methods.

OUMVLP As shown in Tab.2, we also compare our approach with
state-of-the-art gait recognition approaches on OUMVLP, including
GaitNet [48], GaitSet [4], GaitPart [11], GLN [19] and GaitGL [35].
Note that we adopt GaitGL as our baseline and adopt L₈ according
to the guidelines, and the results outperform state-of-the-art gait
by a large margin. The results again demonstrate the effectiveness
of the proposed metric.
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