Broadband near-infrared astronomical spectrometer calibration and on-sky validation with an electro-optic laser frequency comb

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The quest for extrasolar planets and their characterisation as well as studies of fundamental physics on cosmological scales rely on capabilities of high-resolution astronomical spectroscopy. A central requirement is a precise wavelength calibration of astronomical spectrographs allowing for extraction of subtle wavelength shifts from the spectra of stars and quasars. Here, we present an all-fibre, 400 nm wide near-infrared frequency comb based on electro-optic modulation with 14.5 GHz comb line spacing. Tests on the high-resolution, near-infrared spectrometer GIANO-B show a photon-noise limited calibration precision of $< 10 \text{cm/s}$ as required for Earth-like planet detection. Moreover, the presented comb provides detailed insight into particularities of the spectrograph such as detector inhomogeneities and differential spectrograph drifts. The system is validated in on-sky observations of a radial velocity standard star (HD221354) and telluric atmospheric absorption features. The advantages of the system include simplicity, robustness and turn-key operation, features that are valuable at the observation sites.

High-resolution spectrographs are invaluable tools in modern astrophysics that allow for a broad scope of applications ranging from exoplanetary science\textsuperscript{1} to cosmology and fundamental physics\textsuperscript{2}. The former relies on astronomical spectrographs for exoplanet detection and characterisation with the radial velocity technique, i.e. detection of Doppler-shifted absorption features in stellar spectra (Fig.1a). Furthermore, high-resolution spectroscopy allows for probing exoplanet atmospheres\textsuperscript{3,4}. Similarly, monitoring spectra of distant astronomical objects enables measurements of the physical constants variability and constraining the nature of the dark matter\textsuperscript{5,6}. Both, radial velocity technique and physical constant measurement, require extremely precise and accurate instruments, e.g. detection of an Earth analogue necessitates a radial velocity precision of $9 \text{cm/s}$ over a period of several years, while a measurement of the Hubble constant requires two decades of quasar monitoring with a precision of $2 \text{cm/s}$. In view of the extend of the science cases that high-precision astronomical spectroscopy addresses, there is a great interest in developing extremely stable instruments capable of detecting radial velocity shifts at the $\text{cm/s}$ level.

Modern astronomical spectrographs use a cross-dispersion scheme that divides the observed spectra into Echelle orders on a detector array (Fig.1b). Wavelength calibration provides a pixel-to-wavelength mapping mapping for the detector array and thus serves as a wavelength reference for the measured spectra. In order to meet the precision requirements, it is essential to use a broadband, well-characterised light source providing a grid of accurately and precisely defined optical lines of uniform intensity with line separations well resolved by the spectrograph. Absolute calibration is crucial for long-term radial velocity monitoring, as it provides a possibility of comparing data from different epochs and instruments. Figure 1c shows different calibration sources and their respective Echelle spectra. Traditionally, gas cells and hollow cathode lamps have been used as wavelength calibrators providing a performance limited to a precision of about $1 \text{m/s}$ due to sparse lines with high dynamic range in intensity, line blending and unstable intensity profile. Alternatively, Fabry-Pérot interferometers (FPI), fed by an intense white light source produce broadband spectra composed of quasi-equidistant lines (Fig.1d). Enclosed in a vacuum chamber with mechanical and thermal stabilisation, FPIs can provide a one-night stability of $10 \text{cm/s}$. However, a long term stability of both, hollow cathode lamps and FPIs, is not guaranteed; ageing of the lamps or mirror coatings as well as limited long term mechanical stability deteriorate their performance.

A solution that can overcome limitations of standard calibration methods is the laser frequency comb (LFC) technology\textsuperscript{7,8,9,10} (Fig.1e). The unprecedented precision and accuracy of these systems has already brought revolutionary progress to the radial velocity field\textsuperscript{11,12,29}. Frequency combs provide spectra composed of narrow, equally spaced emission lines in the frequency domain, with each optical line frequency $f_n$ described by the relation $f_n = n \cdot f_{\text{rep}} + f_{\text{off}}$, where $f_{\text{rep}}$ and $f_{\text{off}}$ are two radio frequencies (RF) - the repetition rate and the carrier-
envelope offset frequency, respectively. The control over both \( f_{\text{rep}} \) and \( f_{\text{off}} \) allows linking the LFC to the cesium-based atomic time and frequency definition resulting in absolute calibration.

There are several approaches for frequency comb generation. Most commonly, LFCs are generated by mode-locked laser (MLLs) that periodically emit femtosecond pulses. Stabilization and referencing of the comb lines to an RF-standard proceeds via \( f-2f \)-self-referencing. As the native repetition rate, i.e. the comb’s line spacing, of MLLs is typically well below 10 GHz, actively stabilised filtering cavities are used to suppress unwanted modes and hence increase the repetition rate to a value resolvable by astronomical spectrographs. Attention must be paid to the suppression of the side modes so as not to introduce shifts in the apparent frequency of the transmitted mode that may lead to systematic errors. A distinct way of generating frequency combs is provided by Kerr-nonlinear optical microresonators. Recent advances in the field were marked by the first demonstrations of microresonator frequency combs used as wavelength calibrators on astronomical spectrographs.

Electro-optical modulation (EOM) of a continuous wave (CW) laser is another alternative technique for generating LFCs. Here, phase modulation of a CW component results in sideband generation with a line spacing given by an external modulation source driving the electro-optic modulators. When driven by a microwave source, EOM-based combs allow for comb line separation in excess of 10 GHz, which is directly compatible with the requirements of astronomical spectrographs. A pioneering demonstration by Yi et al. showed an operation of a electro-optical frequency comb with a repetition rate of 12 GHz on the CSHELL and NIRSPEC spectrographs. More recently, an advanced EOM-based astrocomb system with a line spacing of 30 GHz in the short-wavelength near-infrared was used to demonstrate the intrinsic stability of the HPF spectrograph of \(<10 \text{ cm/s}\) over several days. Notably, this demonstration included the telescope optics, dual-fibre spectrograph illumination as well as data reduction.

In this article, we present a turn-key EOM-based astrocomb with a line spacing of 14.5 GHz spanning over a wavelength range from 1400 nm to 1800 nm. With this system, we demonstrate a calibration precision reaching \(<10 \text{ cm/s}\) as well as validation in on-sky stellar observation. Specifically, the performance of the EOM LFC was tested on the GIANO-B high-resolution spectrograph. In addition to wavelength calibration and spectrograph drift measurements, relative radial velocity measurements of HD221354 were carried out. The LFC is able to precisely track spectrograph drifts, trace subtle instrumental features and provide precise and accurate wavelength calibration for stellar observations.

RESULTS

Setup. The EOM-based laser frequency comb consists of a 1560 nm CW laser sent through a series of synchronised intensity and two phase modulators driven by a microwave (MW) signal generator at 14.5 GHz (Fig. 2). While phase modulation imprints a chirp on the light wave, the intensity modulator carves out the half period of the phase modulation with a quadratic phase change in time. With this scheme, multiple sidebands are generated around the initial CW laser line resulting in a frequency comb with a flat-top spectrum of 5 nm span. By compensating the dispersion via a chirped fibre Bragg grating (CFBG) (approximately 4 ps/nm), the formation of a train of pulses with a duration of about 2 ps is achieved. These pulses are amplified in an erbium-doped fibre amplifier (EDFA) reaching an average power of 3.5
The demonstration of the EOM-based LFC was performed during several days in November 2017 on the GIANO-B spectrograph (Fig.3) mounted on the 3.6 m Telescopio Nazionale Galileo (TNG) at the Roque de los Muchachos Observatory in La Palma, Spain. GIANO-B is a NIR Echelle spectrograph with a resolution of 50'000 covering the wavelength range from 0.95 µm to 2.45 µm. Observed spectra are composed of 50 spectral orders organised on a detector array of 2048 x 2048 pixels (Hawaii2RG). The extent of a single optical frequency on the detector is given horizontally by the spectrograph’s point-spread-function (PSF) and vertically by the size of the entrance slit. An example of a uranium-neon (U-Ne) hollow-cathode lamp spectrum, a standard calibration source, is shown in Figure 3a (120 s exposure time). The spectrum exhibits sparse lines of...
FIG. 3. Spectrometer raw data. a) Echelle spectrum of a uranium-neon hollow cathode lamp. b) Echelle spectrum of the electro-optic modulation-based laser frequency comb. The dark area in the middle of the 49th order corresponds to the suppressed pump laser. c) The vertical extend of each comb line is given by the slit height, the horizontal profile by the spectrometer’s point-spread-function. d) 1-dimensional data obtained by summing the signal in the analogue-to-digital units (ADU) along the slit with a Gaussian fit. e) GIANO-B spectrograph at the Telescopio Nazionale Galileo.

Deriving a wavelength calibration starts with extracting 1-dimensional data for each Echelle order by summing the signal (analogue-to-digital units, ADU) over the inner 20 pixels along the vertical direction of the slit (Fig.3c and d). The position of each comb line is determined by fitting a Gaussian function (corresponding to the instrument’s PSF) followed by ascribing an exact optical frequency determined on the basis of the known frequency comb parameters. The uncertainty on the fitting is generally below 100 MHz (2% of the PSF’s linewidth), the error being due to fundamental photon noise. The result of assigning comb-frequencies to pixel-positions is shown in Figure 4a. Subtracting a third order polynomial from the data (for visibility) reveals subtle structures related to particularities of the spectrograph optics and detector (Fig.3b and c). Most notably, one can observe a discontinuity in the middle of each order (Fig.3b). This results from the GIANO-B detector being actually a mosaic of four 1024 x 1024 pixel detectors. In the middle of every order there is a discontinuity in the frequency-vs-pixel function due to the detector stitching inducing micrometer deviations in the regular pixel arrangement.

Finally, the wavelength solution, i.e. a complete pixel-to-optical frequency mapping is derived by fitting the data shown in Figure 4a. We employ bounded optimal knots (BOK) free-knot splines method that is based on the algorithm developed by Molinari et al. The Python implementation of this algorithm is provided by the PyCS Python package. Regular spline regression divides the data into parts and fits each section using a low order polynomial that is relied to other sections by knots. The advantage of the BOK free-knot-splines is its improved knot-position optimisation. The algorithm minimizes the χ² by adjusting spline knots positions and fits sections of data with a third order polynomial, taking also into account errors at each data point. This algorithm proves to be an excellent tool in fitting highly variable data (e.g. in the analysis of quasar time series), capturing well the structures in the data without over-fitting (cf. Fig.4b). The (BOK) free-knot splines are applied to each order separately and generate a frequency vs pixel function for each of 2048 pixels for every order.
covered by the LFC. This provides a wavelength solution which corrects for spectrograph imperfections.

One way of determining the calibration precision is comparing two consecutive wavelength calibrations. Here, we consider two wavelength solutions that are separated in time by 2 minutes. For each order, a mean value of the pixelwise differences between the wavelength calibrations is calculated; the standard error for each order is estimated based on the number of statistically independent calibration points (i.e. the number of comb lines). The global drift of the spectrograph is given by a weighted mean over all orders and the precision by the standard error of the weighted mean. The measured spectrometer drift was $70 \pm 14 \text{ cm/s}$ indicating a global precision of $< 10 \text{ cm/s}$ for an individual wavelength solution, fulfilling in principle the requirements for Earth-like planet detection (if all pixels are treated as independent values a precision of $3.5 \text{ cm/s}$ would result). This value is an upper-limit estimation on the wavelength calibration precision, as it also contains the intrinsic spectrograph instability. We point out that reaching this level of precision in practice largely depends on the observation conditions, the coupling of the star light into the spectrometer as well as the global and differential drift rate of the spectrograph. Note that order 49 is excluded from the analysis due to the spectral hole stemming from the not-optimized pump suppression.

**GIANO-B drift measurements.** Next, the spectrograph’s drift is investigated by taking frequent LFC exposures during several hours. The first part of the experiment consisted in alternating the LFC and U-Ne exposures followed by a series of only LFC exposures. The results of the drift measurement are presented in Fig.4. Both, the LFC and U-Ne lamp based wavelength calibrations agree with each other and show the same drift with the LFC resulting in significantly more precise values (reduced scatter).
Additionally, we performed an analysis of a possible wavelength-dependent differential drift of the spectrograph. The insets in Figure 5 show a detector view for three chosen LFC exposures well separated in time. The results show that the right part of the detector drifts at a different rate than the left part during a phase of global linear drift. The wavelength-dependent drift pattern changed after the spectrograph steadied and started to drift in the other direction. The observed effect may be due mechanical drift of the spectrograph and/or thermal regulation of the detector. These results show that the LFC is not only capable of following very precisely the spectrograph’s global drift, but it also provides a detailed map of differential drifts which are a valuable insight into the characteristics of the spectrograph.

On-sky observations. We could benefit from two slots for observations of HD221354 - a nearby K-type star with a visible magnitude of 6.7 and a constant radial velocity within $\pm 2$ $m/s$ [19,21]. The observations were separated in time by 48 hours and each stellar observation (10 min exposure) was bracketed by two LFC exposures (10 s exposure each). A linear drift of the instrument during the stellar exposure is assumed, so that the final wavelength calibration for the stellar data is the mean value of the respective bracketing exposures. Deriving radial velocities from the stellar data is not a straightforward task, as the observed spectra are composed of not only stellar absorption features but also telluric lines - absorption features caused by the Earth’s atmosphere. Separating telluric and stellar absorption features is a first step to undertake for extraction of radial velocities. To do so, we use the synthetic telluric spectra as provided by TAPAS (Transmissions Atmosphériques Personnalisées Pour l’Astronomie) at the specific time, location and meteorological conditions. Figure 5a shows a section of the stellar, TAPAS and LFC spectra. The TAPAS spectrum accurately predicts positions and contrast of telluric lines making it a well-suited tool for generating a mask with which the observed spectrum can be divided into stellar and telluric parts. Next, for both interference-free stellar and telluric spectral portions, the algorithm finds positions of lines and fits a Gaussian. Relative radial velocities between the two observations are determined for every absorption line; for the telluric radial velocity distribution yielding apparent relative radial velocity shifts of $+32$ $m/s$ for the telluric and $-536$ $m/s$ for the stellar spectrum. The latter reflects the difference in Earth’s barycentric velocity between the two observational epochs of $-544$ $m/s$.

Based on the observed lines, an apparent radial velocity shift of $-536$ $m/s$ is measured for HD221354, while $32$ $m/s$ is found for the telluric lines. These are close to the expected values for a correctly calibrated spectrometer. The apparent change in the star’s radial velocity results from the difference between the Earth’s barycentric velocity, equal to $-544$ $m/s$ between the two observations, whereas close to zero shift is expected for the telluric lines in the atmosphere (co-moving with the telescope and only subject to changes in meteorological conditions). The error on the radial velocity shifts for the telluric lines results mainly from the error introduced by the spectrograph slit where a few tens of $m/s$ is expected due to inhomogeneous illumination of the slit caused by imperfect telescope pointing and guiding. The distribution of relative radial velocities for stellar lines is significantly larger than for the telluric lines, which we attribute to the blending between stellar lines with imperfectly masked telluric lines. We anticipate that a dedicated mask for stellar lines, that was not available for this star, can sig-

![Figure 5](image-url)
nificantly reduce the scatter found for the stellar lines to the level obtained for the telluric lines. It is noteworthy that with regard to the on-sky observations the calibration performance is not limited by the LFC but corresponds to the inherent performance limit of the slit-illuminated GIANO-B spectrograph in conjunction with telescope pointing and observational conditions as well as challenges in the data analysis.

**CONCLUSION**

To summarise, we demonstrated broadband astronomical spectrograph calibration of an EOM based laser frequency comb. Notably, the frequency comb is adjustment-free owing to its polarization maintaining all-fibre design that does not include free-space elements such as filtering cavities, spectral equalisers or wave-shapers. Turn-key operation enables start-up times of a few minutes from a powered-off state to a fully phase-coherent GPS- and atomic-clock-referenced state. The actual calibrated wavelength range of nearly 400 nm results in a photon-noise-limited calibration precision of $<10 \, \text{cm/s}$ on the high-resolution near-infrared GIANO-B spectrograph significantly outperforming the currently used standard calibrator (uranium-neon hollow-cathode lamp). In particular, the precise measurement of the spectrograph drift reveals fine structures of the wavelength calibration, i.e. detector inhomogeneities and differential instrument drifts, impossible to grasp with standard calibration methods. Importantly, we could also for the first time validate the performance of an EOM-comb in on-sky observations of the radial velocity standard HD221354 and telluric atmospheric absorption features.

Without compromising on simplicity and robustness, an even larger spectral span could be covered by using stronger phase modulation and higher-power optical amplification along with all-fibre femtosecond pulse compression, as we demonstrate here. In this case an optical microwave-noise suppression stage would need to be inserted into the system in order to achieve narrow comb lines in the far out wings of the spectrum, known from octave spanning combs. Alternatively, with the existence of CW lasers, amplifiers and electro-optic modulators at both edges of the NIR band, it is conceivable to duplicate the system at 1 µm and/or 2 µm in order to increase the spectral coverage. In conclusion, the demonstrated EOM-technology is a uniquely suited tool for spectrometer calibration not only for its performance but notably its robustness and low operational complexity. It is of immediate relevance for the next generation of astronomical precision instruments but also of high interest to a large number of existing instruments that currently use gas lamps as calibrators.

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