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Hot Deformation Behaviour and Processing Map of Cast Alloy 825
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Alloy 825 is a nickel-based alloy that is commonly used in applications where both high strength and corrosion resistance are required, such as tanks in the chemical, food and petrochemical industries and oil and gas pipelines. Components made from Alloy 825 are often manufactured using hot deformation. However, there is no systematic study to optimise the processing conditions reported in literature. In this study, a processing map for as-cast Alloy 825 is established to maximise the power dissipation efficiency of hot deformation in the temperature range of 950 to 1250 °C at an interval of 50 °C and strain rate range of 0.01 s⁻¹ to 10.0 s⁻¹ to a true strain of 0.7 using a Gleeble-3500 thermomechanical simulator. The processing conditions are also correlated to the Vickers hardness of the final material, which is also characterised using optical microscopy and scanning electron microscopy, including electron backscattered diffraction. The true stress-strain curves exhibit peak stresses followed by softening due to occurrence of dynamic recrystallization. The activation energy for plastic flow in the temperature range tested is approximately 450 kJ mol⁻¹, and the value of the stress exponent in the (hyperbolic sine-based) constitutive equation, \( n = 5.0 \), suggests that the rate-limiting mechanism of deformation is dislocation climb. Increasing deformation temperature led to a lower Vickers hardness in the deformed material, due to increased dynamic recrystallization. Raising the strain rate led to an increase in Vickers hardness in the deformed material due to increased work hardening. The maximum power dissipation efficiency is over 35%, obtained for deformation in the temperature range 1100-1250 °C and a strain rate of 0.01 s⁻¹ - 0.1 s⁻¹. These are the optimum conditions for hot working.

### Keywords
- alloy 825
- activation energy
- dynamically recrystallized
- grain size
- hot deformation
- stress-strain curve

### 1. Introduction

Alloy 825 is a solid solution hardening nickel-based alloy (Ref 1) that is used widely in various applications at elevated temperatures under high stress and in corrosive environments, such as tanks in the chemical and oil and gas industries, agitators and heat-exchanger systems (Ref 1, 2). The mechanical and electrochemical properties of the alloy depend on the final grain size. During hot working of nickel-based superalloys and other austenitic alloys, the dominant metallurgical phenomenon is usually dynamic recrystallization, which counteracts the strain hardening caused by the mechanical working of the material and leads to grain refinement (Ref 3-5). However, dynamic recovery also occurs and reduces dislocation density, in competition with recrystallization, without refining grain size. Recrystallization can be detected due to an increase in the

### Abbreviations

| Symbol | Description |
|--------|-------------|
| \( \Sigma \) | A coincidence site lattice value |
| \( \sigma_c \) | A critical stress, MPa |
| \( \varepsilon_c \) | A critical strain |
| \( \theta \) | The strain hardening rate, MPa |
| \( \sigma_p \) | Peak stress, MPa |
| \( \varepsilon_p \) | Peak strain |
| \( Z \) | Zener-Hollomon parameter, s⁻¹ |
| DDM | Dynamic Materials Modelling |
| \( P \) | A total deformation power applied to the material, Joule |
| \( G \) | Power dissipation into plastic flow, Joule |
| \( J \) | Power dissipation into metallurgical phenomena |
| \( \eta \) | The parameter of the efficiency of power dissipation, % |
| \( \xi \) | Metallurgical instability during plastic flow |
| \( a, b, \) and \( c \) | Temperature-dependent strength parameters |
| \( \sigma \) | True stress, MPa |
| \( \dot{\varepsilon} \) | Strain rate, s⁻¹ |
| \( T \) | Deformation temperature, K |
| \( R \) | The universal gas constant, 8.314 J mol⁻¹ K⁻¹ |
| \( Q_{\text{inh}} \) | The apparent activation energy for deformation, J mol⁻¹ |
| \( A A', n, \beta, \beta', \) and \( \alpha \) | Material constants |
| \( \dot{\alpha} \) | Strain rate sensitivity |
| EBSD | Electron Backscattered Diffraction |
| OIM | Orientation imaging microscopy |
| GOS | Grain Orientation Spread, ° |
| PSN | Particle Stimulated Nucleation |
formation, fracture or internal cracking or dissolution of drive metallurgical phenomena, such as dynamic recovery, void dissipation to perform plastic flow, deformation can be considered in two parts: the power to the concept of avoiding areas prone to cracking or other failure (Ref9, 38, 39-43). Previous investigations on Alloy 825 were focused mainly on Cr23C6 precipitation (Ref52, 53) and quantifying corrosion resistance (Ref2, 54, 55), while the study of hot deformation behaviour has received relatively little attention (Ref13, 56, 57). The present work analyses the dependence of flow behaviour on strain rate and temperature. From this, a processing map based on dynamic materials modelling is developed (Ref50, 58). With such a map, it would be possible to find the optimum hot working processing windows for Alloy 825 and optimise the microstructure in the hot-worked material.

1.1 Establishment of Constitutive Equation (Kinetic Analysis)

The relation between the true stress (σ), strain rate (ε) and deformation temperature (T) can be given by equating a constitutive hyperbolic-sine-type equation incorporating stress and the Zener-Hollomon parameter, Z, an Arrhenius-type expression incorporating strain rate and temperature (Ref11, 59-66) (Eq1, where A, n and z are material constants that vary with stress, R is the universal gas constant, 8.314J mol⁻¹K⁻¹, T is the absolute temperature, Zs inh is the apparent activation energy for deformation, î is the strain rate, and σ is the peak true stress).

\[ Z_{\sinh} = \dot{\varepsilon} \exp \left( \frac{Q_{\sinh}}{RT} \right) = A [\sinh(\alpha T)]^n \]  

(Eq 1)

When the argument of the hyperbolic sine function is small, the function approximates to the argument itself (Eq2, where e^x → (1 + x) when x → 0 and so sinh x ≈ x). Conversely, at large arguments, the function tends to a simple positive exponential (Eq2, where e^x → 0 when x is large and so sinh x ≈ ½e^x). Therefore, when ασ < 0.8, Z can be expressed as a power law (Eq3, where A' = Ax^n and the use of the prime symbol (') indicates that each variable relates to this approximate expression and not (1). Taking the natural logarithm of (3 allows the derivation of the unknown materials parameters, A' and n' from the flow curves (Eq4).

\[ \sinh x = \frac{1}{2} (e^x - e^{-x}) \]  

(Eq 2)

\[ Z_\theta = \dot{\varepsilon} \exp \left( \frac{Q_\theta}{RT} \right) = A' \sigma^n \]  

(Eq 3)

\[ \ln \dot{\varepsilon} = \left( \frac{Q_\theta}{RT} \right) + \ln A' + n' \ln \sigma \]  

(Eq 4)

When ασ > 1.2, Z can be approximated by an exponential function (Eq 5, where the double prime (") symbols indicate that the values are associated with the exponential form of the function and not Eq1 or 3). Taking logarithms allows the variables A" and β = ασ" to be derived from flow data (Eq6).

Taking natural logarithm from each side of Eq 5 yields Eq 6, which can be used to extract the unknown material constant β.

\[ Z_\theta = \dot{\varepsilon} \exp \left( \frac{Q_\theta}{RT} \right) = A" \exp(\beta \sigma) \]  

(Eq 5)
\[
\ln \dot{\varepsilon} = \left( -\frac{Q_c}{RT} \right) + \ln A^n + \beta \ln \sigma \quad \text{(Eq 6)}
\]

Similarly, taking logarithms of the original hyperbolic sine relation (Eq 1) have been shown to give a better relation between the Zener-Hollomon parameter and peak stress during hot deformation (Eq 7) (Ref 38, 67-71).

\[
\ln \dot{\varepsilon} = \ln A - \frac{Q_{\text{ sinh}}}{RT} \ln 10 + n \ln[\sinh{(\sigma \rho)}] \quad \text{(Eq 7)}
\]

\( \alpha, \beta \) and \( n' \) are unknown constants that satisfy the relationship \( \alpha = \beta/n' \). The values of \( n \) and \( \beta \) can be derived from the gradients of relevant stress-strain data and substitution of these gradients into Eq 4 and 6.

### 1.2 Establishment of Processing maps (Power Dissipation Maps)

Processing maps are used to model the hot workability window at high temperatures and to predict conditions under which a defect-free (i.e. free of cracks or voids) microstructure may be obtained. The dynamic material modelling approach describes the material behaviour under processing conditions, assuming that the workpiece dissipates power during deformation (Ref 50, 72). During deformation, a total power, \( P \), is applied to the material, which may be divided into \( G \) and \( J \), as described above. As well as leading to shape change, \( G \) may also cause a rise in temperature (Ref 50, 73). The materials phenomena that can account for \( J \) include an increase in dislocation density and grain size (Ref 50, 73). \( P \), \( G \) and \( J \) are, naturally, related and may be expressed in terms of strain rate and instantaneous stress (Eq 8). A **strain rate sensitivity**, \( m \), is defined as the rate of change of energy stored in the microstructure with energy used to perform the deformation (Eq 9) (Ref 29-33, 35, 36, 38-41, 57, 74, 75) and allows the fraction of instantaneous power input that is used to change the microstructure to be calculated (Eq 11). \( m \) has a maximum value of 1 in thermomechanical processing of metals, as a value greater than 1 implies behaviour similar to shear thinning of a liquid, where strain rate increases rapidly with small increments of stress, which is not observed in metals under stable deformation conditions (Ref 49, 72).

\[
P = \sigma \dot{\varepsilon} = \int_0^\sigma \sigma d\varepsilon + \int_0^\varepsilon \dot{\varepsilon} d\sigma = G + J \quad \text{(Eq 8)}
\]

\[
m = \frac{\partial J}{\partial G} = \frac{\sigma \dot{\varepsilon}}{\sigma \dot{\varepsilon}} + \frac{\dot{\varepsilon}}{\sigma} \left( \frac{\partial \dot{\varepsilon}}{\partial \sigma} \right)^{-1} = \frac{\partial \ln(\sigma)}{\partial \ln(\dot{\varepsilon})}
\]

\[
\approx \frac{\Delta \ln(\sigma)}{\Delta \ln(\dot{\varepsilon})} \quad \text{(at a constant \( T \) and \( \dot{\varepsilon} \))} \quad \text{(Eq 9)}
\]

\[
m = \frac{\int_0^\sigma \sigma d\varepsilon}{\int_0^\dot{\varepsilon} \sigma d\varepsilon} = \frac{\sigma}{\sigma \dot{\varepsilon}} \left( \frac{\partial \dot{\varepsilon}}{\partial \sigma} \right)^{-1} = \frac{\partial \ln(\sigma)}{\partial \ln(\dot{\varepsilon})}
\]

\[
\approx \frac{\Delta \ln(\sigma)}{\Delta \ln(\dot{\varepsilon})} \quad \text{(constant \( T \) and \( \dot{\varepsilon} \))} \quad \text{(Eq 10)}
\]

The strain rate sensitivity, \( m \), quantifies the division of power between \( J \) and \( G \), based on the flow stress, \( \sigma \), and strain rate, \( \dot{\varepsilon} \) (Eq 11).

If the flow stress of the workpiece obeys a power law at constant deformation temperature and true strain (Eq 12, Ref 76), it may be called an **ideal dissipator**, and \( J \) reaches a maximum when \( m = 1 \), at which point \( J = G = J_{\text{max}} = \sigma \dot{\varepsilon}/2 \). In this case, the material stores the maximum possible amount of energy in the form of microstructural changes. Such energy can be used to drive recrystallization.

\[
\sigma = k \dot{\varepsilon}^m \quad \text{(Eq 12)}
\]

In the case of workpieces that do not necessarily follow power law, the flow stress in the hot-deformed material varies with strain, strain rate and temperature in a way that is not necessarily linear (Ref 49). In this case, the parameter \( \eta \), called the **efficiency of power dissipation**, is defined. \( \eta \) represents the fraction of the power dissipation that occurs through microstructural changes in the workpiece. It may be defined in terms of \( m \), providing that \( m \) is constant during the deformation (Table 1).

\[
\eta = \frac{J}{J_{\text{max}}} = \frac{\int_0^\sigma \sigma d\varepsilon |_{0 < \sigma < 1}}{\int_0^\sigma \sigma d\varepsilon |_{m = 1}} = \frac{\int_0^\sigma k \dot{\varepsilon}^m d\sigma |_{0 < \sigma < 1}}{\int_0^\sigma k \dot{\varepsilon}^m d\sigma |_{m = 1}} = \frac{m \sigma \dot{\varepsilon}}{m \dot{\varepsilon}} = \frac{2m \sigma \dot{\varepsilon}}{m + 1}
\]

\[
\eta = \frac{J}{J_{\text{max}}} = \frac{\int_0^\sigma \sigma d\varepsilon |_{0 < \sigma < 1}}{\int_0^\sigma \sigma d\varepsilon |_{m = 1}} = \frac{\int_0^\sigma k \dot{\varepsilon}^m d\sigma |_{0 < \sigma < 1}}{\int_0^\sigma k \dot{\varepsilon}^m d\sigma |_{m = 1}} = \frac{m \sigma}{m + 1}
\]

\[
\eta = \frac{J}{J_{\text{max}}} = \frac{\int_0^\sigma \sigma d\varepsilon |_{0 < \sigma < 1}}{\int_0^\sigma \sigma d\varepsilon |_{m = 1}} = \frac{\int_0^\sigma k \dot{\varepsilon}^m d\sigma |_{0 < \sigma < 1}}{\int_0^\sigma k \dot{\varepsilon}^m d\sigma |_{m = 1}} = \frac{m \sigma}{m + 1}
\]

The variation of \( \eta \) with temperature and strain rate constitutes a processing map, which consists of various domains that may be correlated with specific deformation and microstructural evolution mechanisms. Such a map allows the definition of a “safe domain” for processing-conditions under which the material may be deformed without failure. \( \eta \) may be plotted as contour map, based on the deformation temperature and strain rate (Table 2).

Dynamic recrystallization and dynamic recovery are considered to be “safe” microstructural evolution mechanisms, where power dissipation occurs by annihilation of dislocations, and work hardening is avoided or minimised. Of these, dynamic recrystallization is more efficient at removing dislocation density than dynamic recovery and is preferred for hot working.

It is well understood that the high-temperature flow stress behaviour of a given material is strongly dependent on the deformation temperature and strain rate. Numerous studies have suggested different mathematical relations to correlate the flow stress obtained at constant temperature and strain rate. The constant temperature flow stress equation obeys a power law (Eq 12) (Ref 77). Taking natural logarithms of the power law allow the strain rate sensitivity constant, \( m \), to be derived from stress-strain data (Eq 14).

\[
\ln \sigma = \ln k + m \ln \dot{\varepsilon} \quad \text{(Eq 14)}
\]

By comparison with (Eq 14), it may be seen that the first derivative of the quadratic equation with respect to the natural logarithm of strain rate, \( ln \dot{\varepsilon} \), gives the strain rate sensitivity, \( m \), (Eq 15). The peak true stress, \( \sigma_p \), as function of strain rate can also be calculated using a polynomial expression for \( ln(\sigma_p) \) as a function of \( ln(\dot{\varepsilon}) \) for a given deformation temperature (Eq 16, where \( a \), \( b \), and \( c \) are temperature-dependent strength parameters). It was eventually found that a second order polynomial was the most appropriate.
The strain rate sensitivity, $m$, under stable material flow is expressed by the derivative of the natural logarithm of stress with respect to that of strain (Eq 14 cf. Eq 16).

$$m = \frac{\partial \ln \sigma_p}{\partial \ln \dot{\varepsilon}} = b + 2c \ln \dot{\varepsilon} \text{(at constant temperature and strain)} \quad \text{(Eq 16)}$$

When the result of (Eq 17), becomes negative, the flow is predicted to be unstable for the relevant temperature and strain rate (Ref 78).

$$\xi(\dot{\varepsilon}) = \frac{\partial \ln \left( \frac{m}{m + 1} \right)}{\partial \ln (\dot{\varepsilon})} + m = \frac{2c}{m(m + 1)} + m < 0 \quad \text{(Eq 17)}$$

### 2. Material and Experimental Procedure

The material used in this investigation is Ni-based Alloy 825 (composition in Table 1). The material was melted in air in an electric arc furnace, then subjected to argon oxygen decarburization and continuously cast as blooms. The initial microstructure consists of large grains with an average grain size of 430 ± 80 μm (Fig. 1), measured using the linear intercept method. In accordance with ASTM E209, cylindrical compression test pieces were machined with a diameter of 10 mm and a length of 150 mm. The axis of compression was parallel to the long axis of the continuously cast blooms. The samples were machined from a region of the cast where grains were found to be equiaxed.

Isothermal deformation tests were conducted on a Gleeble-3500 thermomechanical simulator (Dynamic Systems Inc. (DSI), New York, NY, USA) at temperatures from 950 to 1250 °C at 50 °C intervals and strain rates range of 0.01 S⁻¹-10.0 S⁻¹ with intervals of an order of magnitude. Tests were performed at Sandvik Material Technology research and development (R&D) department in Sandviken, Sweden. To reduce friction, graphite foil with a thickness between 1 mm and 2 mm was placed on each platen, and a high-temperature lubricant (nickel paste) was applied. In the case of deformation at 1200 °C or 1250 °C, samples were soaked at the deformation temperature for 100 s and then deformed. In the case of samples deformed at temperatures below 1200 °C, samples were first soaked at 1200 °C for 100 s to mimic industrial practice and then cooled at 5 °C S⁻¹ to the deformation temperature. The samples were held at the deformation temperature for 30 s before deformation to ensure a homogeneous temperature.

Samples were compressed by a load of 100 kN under vacuum, before being quenched in high pressure air to a temperature of between 100 and 200 °C. These conditions were selected as it has been shown that the dynamic recrystallization is unlikely to be complete, and the flow stress is likely to be affected by the cast grain structure or grain size (Ref 27, 79). Samples were first homogenised at a temperature between 1200 and 1250 °C and were then compressed to a height reduction of 50%, corresponding to a nominal true strain of 0.7. During testing, barrelling was found to be insignificant under conditions where measurements of peak stress and strain were made.

The deformed samples were cut parallel to the axis of compression and prepared for metallography following standard procedures. The specimens were electrochemically etched for optical microscopy (Zeiss microscopy, Oberkochen, Germany) in a solution of 10 g oxalic acid and 100 ml water for between 3 s and 60 s under an applied potential of 6 V. Quantitative measurement of grain size used the mean linear intercept method. Hardness testing was performed with Vickers method with a 500 g load in accordance with ASTM E384. Five indentations were made for each measurement.

Microstructural investigations were performed on sections parallel to the compression axis using Electron Backscatter Diffraction (EBSD) in a Zeiss Sigma field emission gun scanning electron microscope (Carl Zeiss Microscopy GmbH, Oberkochen, Germany). The data were acquired and processed using the software TSL OIM Analysis version 7 (AMETEK, Inc., Berwyn, PA, USA). Orientation imaging microscopy (OIM) maps and the misorientation angles of grains were calculated from the EBSD data. Grain orientation spread (GOS) was used, instead of a grain size criterion, to classify grains as either recrystallized or deformed (Ref 80-83). This was chosen as a grain size criterion can be misleading, either because dynamic recrystallized grains continue to grow without undergoing deformation at elevated deformation temperature (in which case a recrystallized grain is misclassified as a deformed grain), or parent grains severely fragment at high strain rate (in which case a deformed grain is misclassified as a recrystallized grain) (Ref 81). The GOS is defined as the average difference in orientation between the mean orientation within a grain and the orientation measurement at each point within a single grain (Ref 80-85). Data were cleaned before analysis to minimise the influence of noise on the results. This cleaning consisted of one iteration of grain dilution, with the grain tolerance angle set to 5°. This means that grain boundaries are defined where there is a misorientation of 5° or greater. A minimum grain size of 10 pixels was also defined. When classifying the grains as recrystallized or deformed, a threshold value is defined. In literature, this is selected variously as 1, 2°, 3° or 5° (Ref 80-83, 86). In this study, the initial specimen annealed at 1200°C for

| Elements | Fe  | Cr  | Mo  | Cu  | Ti  | Mn  | Si  | N   | C   |
|----------|-----|-----|-----|-----|-----|-----|-----|-----|-----|
| Content  | 32  | 22.0| 2.5 | 1.6 | 0.8 | 0.7 | 0.2 | 0.009| 0.007|
| Uncertainty | 0.001 | 0.03 | 0.002 | 0.003 | 0.009 | 0.005 | 0.01 |  |

The residue of the alloy is nickel. All values are given in wt.%. Levels of carbon were measured using combustion photometry. Combustion analysis was used for carbon and nitrogen. X-Ray Fluorescence spectrometry was used for other elements. Uncertainty estimates for C and N measurements are taken from data in standard ASTM E1018-11. The uncertainty estimates of the other elements are taken from ASTM E572-13.
100 seconds was examined, as it is undeformed and so contains no deformed grains. It exhibits GOS ≺ 1.3°. The deformed specimens exhibit a broad distribution of GOS, including data above 1.3°, which signifies the presence of deformed grains. This value is consistent with an example from a similar study previously reported in literature (Ref 87). It is reasonable to use a threshold value of 1.3°, or slightly larger to account for the possibility that some recrystallized grains could have slightly higher GOS than was observed in this specimen. Therefore, in this study, a threshold value of 2.0 μm was selected. Also, deformed grains are surrounded by low-angle grain boundaries, which are defined as those boundaries that exhibit a boundary rotation angle of between 2° and 10°; grain boundaries with a rotation angle higher than 10° are defined as high-angle boundaries (Ref 7).

At least 2 maps (1734 μm × 2322 μm) with a step size of 2 μm were analysed to ensure statistical significance. All microstructures and data reported in this study are representative of the respective samples. Grain size was measured from the EBSD maps using the mean linear intercept method. The EBSD data were obtained with a step size of 2.0 μm for the undeformed material and 0.05 μm for the sample deformed at 950 °C at a strain rate of 10 s⁻¹.

### Table 2 Materials constants used in (Eq 16), derived from regression analysis, including the standard error of regression

| Temperature, °C | b       | c       |
|----------------|---------|---------|
| 950            | 0.026 ± 0.021 | 0.08 ± 0.06 |
| 1000           | 0.017 ± 0.013 | 0.04 ± 0.04 |
| 1050           | 0.013 ± 0.010 | 0.05 ± 0.05 |
| 1100           | 0.017 ± 0.017 | 0.05 ± 0.05 |
| 1150           | 0.013 ± 0.010 | 0.05 ± 0.05 |
| 1200           | 0.013 ± 0.010 | 0.05 ± 0.05 |
| 1250           | 0.012 ± 0.011 | 0.04 ± 0.04 |

3. Results

#### 3.1 True Stress-True Strain Curves

True stress-true strain curves were obtained for different combinations of strain rates and temperatures (Fig. 2). The measured total strain in all cases was 0.68 ± 0.04. There is an evident work hardening at the initial stage of the deformation, and the rate of work hardening decreases with increasing strain and eventually reaches a peak. The maximum stress (peak stress) increases with increasing strain rate and decreasing temperature. At temperatures above 1100°C, the stress-strain curves exhibit a peak in flow stress, followed by a slow strain softening and eventually reach a steady state. Test conditions were chosen to prevent significant barrelling in the strain range in which critical stress and strain occurred. During tests, no barrelling was observed until a strain of 0.4-0.5, above which it was minimal (flow stress changed by less than 1% between a strain of 0.4 and 0.7). Therefore, stress-strain data were not
corrected for barrelling, although a correction was applied to account for the compliance of the machine, which was quantified by running a calibration procedure.

3.2 Evaluation of the Constitutive Equation

A second order polynomial was fitted to experimental stress-strain data by least squares regression to interpolate the data and thereby increase the number of datapoints (Ref 78). Plotting the relevant quantities allows the values of the materials constants: $z$, $n$, $Q_{\sinh}$ and $A$. Averaged over all experiments, $z = 7.083 \pm 1.183 \times 10^{-3}$ MPa$^{-1}$, $n = 4.774 \pm 0.146$ (Fig. 3a), $Q_{\sinh} = 542 \pm 17$ kJ mol$^{-1}$ (Fig. 3b) and $(1.55 \pm 0.11) \times 10^{16}$ s$^{-1}$ (Fig. 3c).

The logarithmic plot of Zener-Hollomon parameter against a function of peak stress (Fig. 3c), all experimental points lie on same straight line, suggesting that the materials-dependent constants are indeed constant throughout this study. This implies that one deformation mechanism acts in all conditions, and a constitutive equation for the deformation of Alloy 825 can be written (Eq 18, where the strain rate, $\dot{\varepsilon}$, is expressed in units of s$^{-1}$, the temperature is expressed in Kelvin and the stress in MPa).

$$Z = \dot{\varepsilon} \exp \left( \frac{452400}{RT} \right) = 1.55 \times 10^{16} \sinh(0.00708\sigma_P)^{4.774}$$

(Eq 18)

Similarly, the flow stress can be re-written as a function of Zener-Hollomon parameter by rearranging Eq 1 to give 19.

$$\sigma = \frac{1}{z} \ln \left\{ \left( \frac{Z}{A} \right)^{\frac{2}{n}} + \left[ \left( \frac{Z}{A} \right)^{\frac{2}{n}} + 1 \right]^{\frac{1}{2}} \right\}$$

(Eq 19)

Substituting the value derived for each parameter gives the constitutive equation of equiaxed deformed samples at peak strain, $\dot{\varepsilon}_p$ (since these values were derived using the peak stress) (Eq 20).

$$\sigma_p = 141 \ln \left\{ (3.97 \times 10^{-4})Z^{0.21} + \left[ (1.58 \times 10^{-7})Z^{0.42} + 1 \right]^{1/2} \right\}$$

(Eq 20)

3.3 Quantification of the Process Map

Plotting the natural logarithm of peak stress against that of strain rate (Fig. 4) allows the derivation of the gradient, which is the strain rate sensitivity, $m$ (Eq 16). This may be used to derive the materials constants $b$ and $c$ (Eq 16). The results are summarised in. The strain rate sensitivity can then be used to calculate the efficiency of power dissipation for each deformation condition. According to dynamic materials modelling, one can draw different processing maps with the $\eta$ calculated with Eq 13, 15 or 16. Datapoints on the map were interpolated form the measurement data using the software MATLAB (version 2020b) based on a cubic spline and least squares polynomial regression. For simplicity, the entire processing map has been interpreted as containing four major domains which are marked as I-III and “instability”.

Optical microscopy revealed that the as-deformed microstructures are dominated by an austenitic matrix and are free from intermetallic phases; the only precipitate found was primary TiN (Fig. 6a-d). After deformation at a temperature of 1150 °C and a strain rate of 0.01 s$^{-1}$, the material contains
coarse grains with a high proportion of high-angle grain boundaries (Fig. 6a). After the material was deformed at a temperature of 1100 °C and a strain rate of 0.1 s^{-1}, an elongated structure and small recrystallized grains were observed (Fig. 6b). However, necklace structures, serrated grain boundaries, non-recrystallized deformed grains and grains formed by particle stimulated nucleation (PSN) could be observed following deformation at lower temperatures (Fig. 6c and d). Following deformation at the lowest temperature studied (950 °C), and the highest strain rate studied (10 s^{-1}), electron backscatter diffraction (EBSD) data (Fig. 7) were analysed and indicated the presence of subgrain boundaries (Fig. 7a). This is likely to result in localised work hardening and unstable deformation. Another example to fully illustrate the instability, deformed grains dominated the entire equiaxed structure, as shown in Fig. 7b. Grain orientation spread analysis was used to identify grains that were recrystallized (Table 3).

3.4 Hardness Measurements

Vickers hardness was measured in samples as a function of deformation strain rate and temperature (Fig. 8). The datapoints in the map were interpolated using a cubic spline and least squares regression in the software MATLAB (version 2020b).

4. Discussion

4.1 Stress-Strain Behaviour

The flow behaviour indicated by Error! Reference source not found. is in agreement with the results of previous investigations (Ref 27, 79, 88). An existing model proposes that dynamic recovery consists of two competing processes: the generation of dislocations and the annihilation of dislocations (Ref 6, 49, 89). The relative rate of these two processes will determine the shape of stress-strain curves: if the rate of dislocation annihilation is larger than that of generation, it will result in flow softening. If dislocation annihilation is slower than dislocation generation, flow stress will continuously increase and lead to work hardening. If a balance is established between these two rates, a steady flow stress can be observed. The results indicate that all conditions led to initial work hardening, but that a balance was established in most cases (Fig. 2). This is common for hot deformation of metals. In some cases, work hardening persisted for the entire deformation. This was favoured by low temperatures and high strain rates (e.g. 950 °C and 1.0 s^{-1}). Conversely, high temperatures favoured strain softening, especially at low strain rates.

4.2 Constitutive Equation Analysis

The value of $n = 4.774$ (Fig. 3a) indicates that the deformation is governed by the glide and climb of dislocations, in which case theory predicts that $n = 5$ (Ref 90). The activation energy for plastic deformation, $Q_{\text{sinh}} = 452 \pm 17 \text{ kJ mol}^{-1}$ is quite close to that reported in the previous study on the deformation activation energy reported by the same authors (Ref 30). This value is also within the range of activation values reported for nickel-base
superalloys: 416.6 kJ mol\(^{-1}\) (Ref 91), 438 kJ mol\(^{-1}\) (Ref 92), 450.8 kJ mol\(^{-1}\) (Ref 74), 451 kJ mol\(^{-1}\) (Ref 75), 465 kJ mol\(^{-1}\) (Ref 20), 472 kJ mol\(^{-1}\) (Ref 76) and 486 kJ mol\(^{-1}\) (Ref 13). However, it is higher than values obtained for this alloy in other studies: 438 kJ mol\(^{-1}\) (Ref 92) and 416.6 kJ mol\(^{-1}\) (Ref 91). The former used peak stress data measured in wrought samples of a different size to the current study and the latter in extruded material. Neither can be compared with confidence to the current study and both lie within the range of deformation activation energy listed above. The deformation of nickel-based alloys is usually controlled by the climb of dislocations around obstacles (Ref 20). The measured activation energy in the current study is greater than the activation energy of self-diffusion in nickel (280 kJ mol\(^{-1}\)) (Refs 46, 73). This implies that some other mechanism is limiting. Moreover, the activation energy for deformation is affected by peak stress, \(\sigma_P\) and stress exponent, \(n\) (Eq 7). Both \(\sigma_P\) and \(n\) are related to microstructural features such as precipitates and grain size. As a result, the activation energy for deformation must also vary with the microstructure, which reflects the complex interaction between the kinetics of the various processes by which dislocations are generated, annihilated and pinned (Ref 93). Precipitates can inhibit dislocation glide, dislocation climb and grain boundary movement, and it is known that Alloy 825 contains precipitates. Thus, the mean value of the deformation activation energy for Alloy 825 is much larger than the self-diffusion activation energy of pure nickel.

### 4.3 Efficiency of Power Dissipation and Microstructural Analysis

A strain of 0.7 represents the situation at flow softening state or the steady state, depending on the deformation temperature (Fig. 2). The efficiency of power dissipation, \(\eta\), is dependent on the strain rate sensitivity index, \(m\), and the microstructural changes during deformation (Eq 9 and 13). Therefore, it follows that microstructural evolution can be predicted by analysing the value of \(\eta\) (and validated using metallography). The domains in processing maps can also be characterised based on the resulting microstructure [18]. The power dissipation maps developed at the strain of 0.7 exhibit four different domains with relatively high peak efficiencies of power dissipation.
dissipation (Fig. 5). It is worth noting that there is enough time for nucleation and growth process at the lowest strain rate (0.01 s⁻¹). This is reflected in the fact that the volume fraction of dynamically recrystallized grains at low strain rates is significantly larger than at higher strain rates (Fig. 6a, Table 3).

The processing map (Fig. 5) exhibits four different domains of deformation efficiency in the temperature and strain rate ranges. Domain I describes the range of conditions in which large (23.5 ± 1.4 μm) dynamically recrystallized grains form (e.g. Fig. 6(a)). Because the mobility of grain boundaries is enhanced as solute drag diminished with increasing deformation temperature (Ref 6). This is consistent with hot-worked Ni20Cr (grain size ≈ 45μm) in previous studies, which show a peak efficiency of approximately 38% at a total true strain of 0.5, deformation temperature of 1200 °C and a strain rate of 0.1s⁻¹ (Ref 5). Similar alloys begin recrystallization with the formation of twins (Ref 8).

Domain II exhibits a power dissipation efficiency value (25%-30%) between values typical of full dynamic recovery (15%-25%) and pure dynamic recrystallization (30-40%), which implies that both mechanisms are active simultaneously and compete with each other. A typical microstructure in domain II shows many elongated grains and a large number of small (6.5 ± 0.1μm) recrystallized grains (Fig. 6b). Grain boundary mobility is lower than in Domain I, and the faster strain does not allow grain boundaries to move during deformation. Therefore, no significant grain growth was observed in domain II. Adiabatic heating of the samples has been suggested as a mechanism that contributes to strain softening effects under such conditions (Ref 94).

Domain III represents temperatures between 950 and 1100 °C and strain rates above 0.1 s⁻¹. The microstructure is inhomogeneous with serrated grain boundaries and necklace structures (e.g. Fig. 6c). The necklace structure is indicative of grain boundary bulging, which suggests ongoing recrystallization. This is consistent with observed trends in a nickel-base superalloy similar to the alloy being studied here (Ref 95). Under the conditions of low or moderate temperature and high strain rate, a very high dislocation density will be developed, which will provide many nucleation sites for, and increase the driving force of, recrystallization (Ref 18, 50). This leads to the conclusion that the fine grain structure is caused by extensive nucleation of dynamically recrystallized grains, but grain growth is limited by the short deformation time and limited temperature.

The material exhibits flow instability below 1100 °C and at a strain rate above 0.3s⁻¹. The microstructure exhibits a substructure that formed during the deformation, eliminating the possibility that recrystallization occurred. This is consistent with a previous study, in which a similar substructure dominates the material (Ref 79). In addition, some heavily deformed structures were found to be localised (Fig. 7a). This occurs because flow stress localization easily occurs at high strain rates, where dislocations form easily in regions already

Fig. 7 EBSD images (band contrast) of equiaxed compressed specimen of an Alloy 825 after a uniaxial compression to a nominal strain of 0.7 and a strain rate of 10 s⁻¹ at the deformation temperature of 950 °C. (a) 500x magnification (b) 50x magnification, each overlaid with high-angle (black) and low-angle (white) grain boundaries. A colour version of this figure is available online.
containing a high dislocation density (Ref 38, 46). Dispersed particles of titanium nitride (TiN) are present, and dislocations were especially dense around such particles during deformation (Fig. 7a). This was also observed in a previous study (Ref 27). When the size of a TiN particle is greater than 0.5 \( \mu \text{m} \), they can stimulate dynamic recrystallization, which was observed here (Fig. 6d) and is referred to as particle stimulated nucleation (Ref 6).

There is no distinct (sharp) boundary between these domains and the exact values at which the boundaries between domains were defined in Fig. 5 that are taken at convenient values of the power dissipation efficiency, although they are appropriate according to the definitions above. The instability domain was defined to exist where the power dissipation efficiency was below 20%. Domain III was defined at values between 20% and 25%, domain II between 25% and 30% and domain I above 30%.

Therefore, for Alloy 825, it is preferable to conduct any hot working at a temperature between 1100 and 1250 °C at a strain rate between 0.01 and 1.0 s\(^{-1}\) (Domain I). This gives the highest achievable power dissipation efficiency. It is necessary to avoid working the alloy in the temperature range of 950-1100 °C for a strain rate of above 0.3s\(^{-1}\), as this leads to “instability”. This is because dynamic recrystallization may not be completed under such conditions (Fig. 6a cf. Fig. 6d).

The model used in the current study does not clearly define the partial and/or non-recrystallized regimes. Significant advances in the understanding of microstructural refinement through thermomechanical processing have shown different ways to produce a well-conditioned microstructure during hot deformation. Therefore, the combined use of hot deformation maps using the Dynamic Materials Modelling approach and the application of well-known physical models, such as those that account for recrystallization, total strain and temperature or recrystallization, and time can provide a powerful tool to the understanding of microstructural optimization through thermomechanical processing. The power dissipation efficiency, \( \eta \), is an important parameter for the determination of the extent of power dissipation by microstructural changes during hot deformation. The optimum hot working condition is when \( \eta \) is maximum, and the maximum possible energy is stored as microstructural changes, such as recrystallization and recovery.

### 4.4 Hardness

It is evident that hardness depends strongly on deformation temperature and strain rate (Fig. 8). These results are in agreement with the dynamic material model (Fig. 5). The hardness values for compressed specimens increases with decreased deformation temperature and increased strain rate. This is because increasing the temperature leads to more extensive recrystallization (Table 3, Fig. 6). This will remove dislocation density and lead to softening. An increase in strain rate reduces the total time available for recrystallization. Strain hardening arises from the formation of a substructure of dislocations in the matrix (Fig. 7) and leads to a higher hardness (225 HV0.5). No void formation occurred at the hard titanium nitride (TiN) particles (Fig. 6d). Additionally, it is suggested that the processes of recrystallization and recovery are active and influence the softening of the material.

### 5. Conclusions

The hot deformation behaviour of the equiaxed-grain specimens of continuously cast blooms of Alloy 825 was investigated. Deformation occurred at temperatures between 950 and 1250 °C and at strain rates from 0.01 to 10.0 s\(^{-1}\). The efficiency of power dissipation and the hardness of the resulting microstructures were assessed.

1. The flow stress is both strain rate and temperature-dependent. It increases with increasing strain rate and decreasing temperature. The peak true flow stress of Alloy 825 can be represented by the following equation:

   \[
   Z = \dot{\varepsilon} \exp\left(\frac{Q_{\text{inh}}}{RT}\right) \approx A [\sinh(\alpha \dot{\varepsilon})]^n
   \]

2. The average activation energy for hot deformation, \( Q_{\text{inh}} \), was determined to be 450kJmol\(^{-1}\). The average value of \( \alpha \) was determined to be 7.1 \times 10^{-3}. The hot flow beha-

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**Table 3 Extent of recrystallization in selected samples from the current study**

| Deformation temperature, °C | Strain rate, s\(^{-1}\) | Percentage of grains that were recrystallized |
|-----------------------------|-------------------------|---------------------------------------------|
| 1150                        | 0.01                    | 44                                          |
| 1100                        | 0.1                     | 14                                          |
| 1000                        | 10.0                    | 7                                           |
| 950                         | 10.0                    | 2                                           |

Both high temperature and low strain rate promote recrystallization.
virion can be described well by the hyperbolic-sine-type equation. The mean creep exponent, $n$, was found to be a close to value of 5 hence the hot deformation in equiaxed compressed specimens is governed by the glide and climb of dislocations.

(3) In the process map, a domain at a deformation temperature of between 1100 and 1250 °C, with a strain rate of between 0.01 s$^{-1}$ and 0.1 s$^{-1}$ gives the optimum hot deformation condition. It exhibits a high power dissipation efficiency (up to 35%) and can result in fine recrystallized microstructure.

(4) The hot processing map suggests good workability for a wide range of conditions with a strain rate, $\dot{\varepsilon} < 0.1 \text{s}^{-1}$ and a temperature of 1100 °C or higher.

(5) The optimum processing parameters for good strain hardening are obtained in the temperature range of between 950 and 1100 °C with a strain rate of $0.3 \leq \dot{\varepsilon} \leq 10.0$.

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Data Availability

The raw data required to reproduce these findings are available upon request to the corresponding author. The processed data required to reproduce these findings are available upon request to the corresponding author.

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