WEAK EXPECTATIONS OF DISCRETE QUANTUM GROUP ALGEBRAS AND CROSSED PRODUCTS

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Abstract. In this article we study analogues of the weak expectation property of discrete group C*-algebras and their crossed products, in the discrete quantum group setting, i.e., discrete quantum group C*-algebras and crossed products of C*-algebras with amenable discrete quantum groups.

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