Effective dose calculation at flight altitudes with the newly computed yield function

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An important topic in the field of space weather research is the assessment of the expected exposure of aircrew at flight altitudes due to cosmic rays (CRs), specifically during major solar energetic particle (SEPs) events. The primary cosmic ray particles induce a complicated nuclear-electromagnetic-muon cascade in the Earth atmosphere. The secondary particles form the main source of increased exposure at flight latitudes compared to the sea level. In this work we propose a numerical model for computation of the effective dose at typical commercial flight altitudes. It represents a full chain analysis, namely estimation of the solar particle spectral and angular characteristics from neutron monitor (NM) data and application of the newly computed yield function for the effective dose. The new computed yield functions for conversion of secondary particle flux to dose were obtained on the basis of extensive Monte Carlo simulation of the atmospheric cascade induced by primary protons and alpha particles and subsequent application of recently computed conversion coefficients. A comparison with the reference data is performed. A good agreement is achieved. Several example calculations are demonstrated. An application of the method for assessment of effective dose during several ground level enhancements (GLEs) is shown.

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1. Introduction

The planet Earth is constantly bombarded by high-energy particles (galactic cosmic rays—GCR), mostly protons and \( \alpha - \)particles which penetrate deep into the atmosphere, producing large amount of secondaries. As a result aircrews are subject to increased exposure comparing to the sea level due to the increased intensity of secondary CRs. Another possible source of increasing exposure is due to sporadic source, namely by SEPs, which could produce similar atmospheric cascade, known as GLEs. At recent it was demonstrated that CRs affect the radiation environment and accordingly exposure at commercial flight altitudes, specifically during GLEs [1, 2, 3, 4, 5]. An assessment of aircrew exposure is based on CR measurements and subsequent computations using the derived spectral and angular characteristics. Here, we describe a numerical model to estimate effective dose at flight altitudes, based on newly computed yield functions and reconstruction procedure of SEPs characteristics based on ground measurements with NMs.

2. Model and newly computed yield functions for effective dose assessment at flight altitudes

The dose rate can be computed as a function of the geomagnetic rigidity cut-off and altitude using a full Monte Carlo simulation of the atmospheric cascade [6]. At present, several models have been proposed, aiming to estimate the dose rate (effective and/or ambient dose equivalent) at flight altitudes due to primary CR radiation [7, 8, 9, 10, 11, 12, 13, 14].

Because the effective dose is not a measurable quantity, International commission of radiation protection ICRP suggest the ambient dose equivalent [15] denoted as \( H^*(d) \). It represents the dose equivalent that would be produced by the corresponding expanded and aligned field at a depth \( d \) in a International Commission on Radiation Units and Measurements (ICRU) sphere (a sphere with diameter of 30 cm made of tissue equivalent material with a density of 1 \( \text{g.cm}^3 \) and a mass composition of 76.2 % Oxygen, 11.1 % Carbon, 10.1 % Hydrogen and 2.6 % Nitrogen) on the radius vector opposing the direction of the aligned field. The unit for both effective dose and ambient dose equivalent is Sv. The ambient dose equivalent at a depth of \( d=10\text{mm} \) \( H^*(10) \) is recommended as a reasonable proxy for the effective dose as was shown in [16]. In fact, it slightly overestimates the effective dose, but it is not a conservative estimate for cosmic radiation exposure at aviation altitudes according to [3] and the results work presented here. Nevertheless, it is regarded as an acceptable approximation for effective dose at aircraft altitudes [17, 13].

The effective dose rate at a given atmospheric depth \( h \) induced by a primary CR particle is given by:

\[
E(h, \lambda_m, \theta, \phi) = \sum_i \int_{T'(\lambda_m)}^\infty \int_{\Omega} J_i(T') Y_i(T', h) d\Omega dT'
\]  

(2.1)

where \( T' \) is the energy of the primary CR particle arriving from zenith angle \( \theta \) and azimuth angle \( \phi \), \( J_i(T') \) is the differential energy spectrum of the primary CR at the top of the atmosphere for \( i \) component (proton and/or \( \alpha - \)particle), \( \lambda_m \) is the geomagnetic latitude, \( \Omega(\theta, \phi) \) is a solid angle
and $Y_i$ is the effective dose yield function. The corresponding effective dose yield function $Y_i$ is defined as

$$Y_i(T', h) = \sum_j \int F_{i,j}(h, T', T^*, \theta, \phi) C_j(T^*) dT^*$$  \hspace{1cm} (2.2)$$

where $C_j(T^*)$ is the fluence to effective dose conversion coefficient for a secondary particle of type $j$ (neutron, proton, $\gamma$, $e^-$, $e^+$, $\mu^-$, $\mu^+$, $\pi^-$, $\pi^+$) with energy $T^*$, $F_{i,j}(h, T', T^*, \theta, \phi)$ is the fluence of secondary particle of type $j$, produced by a primary particle of type $i$ (proton and/or $\alpha$- particle) with a given primary energy $T'$. The conversion coefficients $C_j(T^*)$ for a particle of type $j$ are obtained using Monte Carlo simulations \[16, 18\]. The secondary particle flux produced by primary protons and $\alpha$-particles in a wide energy range is obtained on the basis of atmospheric cascade simulations using GEANT4 \[19\] based PLANETOCOSMICS code \[20\]. The yield function considers the complexity of the atmospheric cascade development, since it brings information of particle fluence and spectrum at a given altitude in the atmosphere, considering the secondary particle attenuation. The newly computed effective dose yield function for 35 kft (typical commercial flight altitude $\approx 10.5$ km) is shown in Fig.1.

![Effective dose yield function for protons and $\alpha$-particles](image1.png)  \hspace{1cm} ![Total Effective dose yield function](image2.png)

(a) Effective dose yield function for protons and $\alpha$--particles \hspace{1cm} (b) Total Effective dose yield function

Figure 1: Effective dose yield function as a function of the energy per nucleon for primary CR protons and $\alpha$--particles at 35 kft (altitude of $\approx 10.5$ km).

Details concerning the computation including look-up tables are given elsewhere \[21\].

3. Application of the model

Since the ambient dose equivalent is acceptable approximation for effective dose at aircraft altitudes, we perform a comparison of our model with reference data. The computed effective dose $E$ compared with reference data \[22\] at the altitude of 35 kft a.s.l. for several periods is shown in Fig. 2. Here (Eq. 2.1) we assume the force field model for GCR with the corresponding modulation parameter \[23\]. We achieve a good agreement between the model computations and the reference data.
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Figure 2: Computed effective dose $E$ and reference data [22] at the altitude of 35 kft a.s.l. a) January 1998 b) January 2000 c) January 2002.

During major GLEs, the exposure is a superposition of the contribution of GCRs and SEPs, which possess an essential anisotropic part during the event onset. Therefore, as the first step the spectra SEPs should be determined outside the magnetosphere. In order to consider explicitly the anisotropy we compute the asymptotic cones in the region of interest in a grid of $5^\circ \times 5^\circ$ with the MAGNETOCOSMICS [20].

Here we apply derived spectral and angular characteristics of GLE particles obtained on the basis of NM data [24] using newly computed NM yield function [25]. Details are given elsewhere in this volume. The effective dose rate during various periods of GLE 70 is shown in Fig.3, accordingly for GLE 59 in Fig.4. During the initial phase of GLE 70 the computed effective dose was about 40-50 $\mu$Sv.h$^{-1}$, while during the main and late phases the contribution of SEPs to the dose is comparable to the average due to GCR. The computed effective dose during the initial phase of GLE 59 was about 30 $\mu$Sv.h$^{-1}$. It diminished to about 14 $\mu$Sv.h$^{-1}$ during the main and late phase of the event.

4. Conclusion

Here we present a new full chain analysis model for assessment of effective dose at flight altitudes. The model is based on NM data and newly computed yield functions. The model demonstrates good agreement with reference data for GCRs and it is succesfully applied for computation of effective dose rate during two GLEs. The model is fully operational and could be used for space weather applications.
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Figure 3: The effective dose rate $[\mu\text{Sv h}^{-1}]$ at the altitude of 35 kft a.s.l. during the GLE 70 on 13 December 2006 in a region with $R_c \leq 1$ GV. a) initial phase of the event; b) main phase of the event; c) late phase of the event.

Figure 4: The effective dose rate $[\mu\text{Sv h}^{-1}]$ at the altitude of 35 kft a.s.l. during the GLE 59 on 14 July 2000 in the region with $R_c \leq 1$ GV. a) event onset; b) main phase of the event.
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