Can the Friction of the Nova Envelope Account for the Extra Angular Momentum Loss in Cataclysmic Variables?

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Abstract

It has been shown that the rate of angular momentum loss (AML) in cataclysmic variables (CVs) below the period gap is about 2.47 times that caused by gravitational radiation (GR), suggesting an extra AML mechanism aside from GR. Several potential mechanisms have been proposed but none of them has been verified. In this work, we examine whether AML caused by friction between the expanding nova envelope and the donor star can account for the required AML rate. By adopting various expanding velocities of the envelope, we have calculated the evolution of CVs with typical initial parameters. Our results show that this friction interaction likely solves the extra AML problem unless the expanding velocities are extremely low. Thus, there should be a more efficient AML mechanism that plays a role in CV evolution.

Key words: novae, cataclysmic variables – stars: evolution – white dwarfs

1. Introduction

Cataclysmic variables (CVs) are interacting binaries where a low-mass donor star is transferring material onto a white dwarf (WD; see Warner 1995; Ritter 2010; Knigge et al. 2011 for reviews). The orbital periods of most CVs are \( \lesssim 1 \) day, and the mass transfer is driven by orbital angular momentum loss (AML). In the standard model of CV evolution, AML is dominated by magnetic braking (MB; Verbunt & Zwaan 1981; Rappaport et al. 1983) above the \( \sim 2-3 \) hr period gap, while below the period gap, the donor star becomes fully convective so the effect of MB ceases and only gravitational radiation (GR; Landau & Lifshitz 1975) works.

A study of the CV population led Patterson (1998) to suggest that the AML rate below the period gap may be higher than the traditional prescription, which predicts that most (99\%) of the total CVs populate the short-period regime (Kolb 1993). Knigge et al. (2011) reconstructed the full evolutionary path of CVs based on the observed mass–radius relationship of low-mass stars. Their best-fit results showed that the scaling factors \( f_{\text{GR}} \) and \( f_{\text{MB}} \) for the standard GR- and MB-induced AML rates, respectively, are \( f_{\text{GR}} = 2.47(\pm 0.02) \) below the period gap and \( f_{\text{MB}} = 0.66(\pm 0.05) \) above the period gap. More recently, Pala et al. (2017) investigated the CV evolution using the effective temperatures of the WDs as a probe. They obtained a good fit with the observations provided that there is an additional AML mechanism below the period gap. This mechanism could be residual MB when the donor has no radiative core (Patterson 1998) or consequential AML (hereafter CAML) due to mass loss along with the mass transfer process (Nelemans et al. 2016; Schreiber et al. 2016).

Shao & Li (2012) investigated three possible CAML mechanisms related to mass loss in CVs: (1) isotropic wind from the surface of the WDs (King & Kolb 1995), (2) mass loss through the Lagrangian points \( L_1 \) or \( L_2 \) (Vanbeveren et al. 1998), and (3) the formation of a circumbinary (CB) disk from the outflow (van den Heuvel 1994; Taam & Spruit 2001). They showed that neither isotropic wind nor outflow from the \( L_1 \) point can account for the extra 1.47 times GR-induced AML rate (\( \dot{J}_{\text{GR}} \)), although outflow from the \( L_2 \) point or the formation of a CB disk may account for it, provided that \( \sim 15\%-45\% \) or \( \sim 20\%-40\% \) of the transferred material leaves the binary, respectively. In reality, both isotropic wind and outflow may simultaneously play a role during CV evolution, and Liu & Li (2016) found that the mass transfer in CVs with low-mass WDs becomes dynamically unstable in case the fraction of mass loss in the form of a CB disk is \( \sim 20\%-30\% \).

Another important topic associated with CV evolution is the absence of low-mass WDs in CVs (de Kool 1992; Politano 1996; Zorotovic et al. 2011; Wijnen et al. 2015). To solve this problem, Schreiber et al. (2016) suggested an alternative empirical CAML model taking into account the AML due to the mass transfer in CVs. They carried out detailed CV population synthesis simulations, assuming that the specific AM of the lost matter increases with decreasing WD mass. The results showed that this model could explain the discrepancy between the measurements and theoretical predictions of the average WD mass in CVs, as well as the orbital period distribution (Kolb & Baraffe 1999; Knigge 2006; Gänzicke et al. 2009) and space density distribution (Ritter & Burkert 1986; Kolb 1993; Patterson 1998; Pretorius & Knigge 2012) of CVs. However, the physical origin of this kind of CAML is not known, though it is likely to be related to mass loss during nova eruptions. Schenker et al. (1998) investigated AML due to friction (hereafter FAML) between the expanding nova envelope and the donor star. They showed that the strength of FAML sensitively depends on the expanding velocity of the ejecta at the location of the donor, which is stronger for smaller expanding velocities. Interestingly, previous studies (Livio et al. 1991; Yaron et al. 2005) have shown that expanding velocities are expected to be lower in lower mass WDs than in more massive ones. Therefore, FAML may present a possible explanation for the empirical CAML law suggested by Schreiber et al. (2016). However, whether FAML can explain the extra 1.47\( \dot{J}_{\text{GR}} \) below the period gap still needs to be examined. This is the objective of our work.

The rest of this paper is organized as follows. In Section 2, we describe the input physics and the FAML model considered.
in the binary evolution calculations. The numerically calculated results are presented in Section 3 and compared with the analytic derivation in Section 4. We summarize our results in Section 5.

2. Model

We carried out binary evolutionary calculation of CVs using the Modules for Experiments in Stellar Astrophysics (Paxton et al. 2011, 2013, 2015). Generally, during nova eruptions, all of the material accreted by the WD is ejected. Therefore, there is no net mass accumulation for a WD in CVs. However, at the beginning of mass transfer, there could be a stage of stable hydrogen and helium burning depending on the mass ratio, so we include possible mass accumulation. The mass growth rate $\dot{M}_{\text{WD}}$ of a WD can be described as follows:

$$\dot{M}_{\text{WD}} = -\eta_{\text{H}}\eta_{\text{He}}\dot{M}_2,$$

where $\eta_{\text{H}}$ and $\eta_{\text{He}}$ are the mass accumulation efficiencies for hydrogen and helium burning, respectively, and $-\dot{M}_2$ is the mass transfer rate. We refer to Hillman et al. (2016) and Kato & Hachisu (2004) for the dependence of $\eta_{\text{H}}$ and $\eta_{\text{He}}$ on the WD mass and the mass transfer rate, respectively (see also Liu & Li 2016 for more details). The excess material is assumed to leave the binary at a rate of $(\dot{M}_2 - \dot{M}_{\text{WD}})$, taking away the specific AM of the WD. In particular, if the mass transfer rate is lower than $3 \times 10^{-8} \text{M}_\odot \text{yr}^{-1}$, novae are supposed to take place where all of the accreted material is ejected from the surface of the WD. In this case, besides AML due to mass loss, we also consider possible AML caused by frictional interaction (see below).

In our calculations, systematic AML due to GR (Landau & Lifshitz 1975) and MB (Verbunt & Zwaan 1981) is included. We take the solar chemical abundance ($X = 0.70$, $Y = 0.28$, and $Z = 0.02$) for the donor star.

2.1. Frictional Angular Momentum Loss

Schenker et al. (1998) proposed that FAML may exist between the expanding nova envelope and the secondary. They deduced the FAML expression based on the Bondi–Hoyle accretion model. Since the duration of nova eruptions is much shorter than the mass transfer time, we use their long-term continuous wind average to investigate its influence on the secular evolution of CVs. The mean specific AM $\dot{J}_{\text{ej}}$ of the ejected material during nova eruptions can be written as follows:

$$\dot{J}_{\text{ej}} = (q + \nu_{\text{FAML}})\frac{J}{M},$$

with $q = M_2/\dot{M}_{\text{WD}}$ being the ratio of the donor mass to the WD mass, and $J$ and $M$ the total AM and mass of the binary, respectively. On the right-hand side of Equation (2), the first term represents the specific AM of the WD carried away by the expanding material, and the second term the specific AM related to the friction between the expanding envelope and the donor star. Here, the parameter $\nu_{\text{FAML}}$ represents the strength of FAML,

$$\nu_{\text{FAML}} = \frac{(1 + q)^2}{4q} \left( \frac{R_{1,2}}{a} \right)^2 \nu_{\text{rel}} \nu_{\text{exp}},$$

where $R_{1,2}/a$ is the ratio of the Roche lobe (RL) radius of the donor to the binary separation, $\nu_{\text{exp}}$ the expansion velocity of the envelope from the WD, and $\nu_{\text{rel}}$ the relative velocity of the expanding envelope to the donor star, $\nu_{\text{rel}} = \sqrt{\nu_{\text{sec}}^2 + \nu_{\text{exp}}^2}$, where $\nu_{\text{sec}} = \sqrt{GM/a}$ is the orbital velocity about the WD. Since the donor star cannot spin the envelope up to velocities faster than corotation, we set an upper limit for FAML as in Schenker et al. (1998),

$$\dot{j}_{\text{max}} = \dot{j}_1 + \left( \frac{R_2}{a} \right)^2 \omega,$$

where $\dot{j}_1$, $R_2$, and $\omega$ are the specific AM of the WD, the radius of the donor star, and the angular velocity of the binary, respectively. Therefore, the actual specific AM of the ejecta including FAML is given by

$$\dot{j}_{\text{ej}} = \min(\dot{j}_1, \dot{j}_{\text{max}}).$$

3. Calculated Results

In our calculation, we take the initial WD mass to be $M_{\text{WD,i}} = 0.5, 0.8$, and $1.1 \text{M}_\odot$, and the corresponding initial donor star mass to be $M_2 = (0.4, 0.5, 0.6) \text{M}_\odot, (0.6, 0.8, 1.0) \text{M}_\odot$, and $(0.6, 0.8, 1.0) \text{M}_\odot$, respectively. For the expanding velocity of the ejected envelope, we adopt $\nu_{\text{exp}} = 40, 80$, and $200 \text{ km s}^{-1}$.

In Table 1, we list the calculated results without FAML (i.e., $\nu_{\text{FAML}} = 0$). These results can be used as a reference for comparison with other models. We find that for $M_{\text{WD,i}} = 0.5 \text{M}_\odot$, when $q > 1$, the WD mass can grow to some extent. The reason is that these systems initially experience thermal-timescale mass transfer for some time. In other systems, the mass transfer rates never exceed $3 \times 10^{-8} \text{M}_\odot \text{yr}^{-1}$ during the entire evolution, so they all experience novae. The minimum orbital period $P_{\text{orb,min}}$ ($\leq 70$ minutes) depends on both the WD mass and the initial orbital period $P_{\text{orb,i}}$: the larger $M_{\text{WD,i}}$ and the shorter $P_{\text{orb,i}}$, the is longer $P_{\text{orb,min}}$.

Tables 2–4 present the calculated results by taking FAML into account, with $\nu_{\text{exp}} = 40, 80$, and $200 \text{ km s}^{-1}$, respectively. FAML slightly enhances the mass transfer rate compared with the no-FAML cases. For $M_{\text{WD,i}} = 0.5 \text{M}_\odot$, this leads to more efficient mass growth in the WDs, which increases with decreasing $\nu_{\text{exp}}$. The minimum orbital period $P_{\text{orb,min}}$ is not influenced by whether or not FAML is considered.

In order to show more details of the evolution, Figures 1–3 present three examples for different WD and donor masses. In Figure 1, the initial parameters are $M_{2,i} = 0.6 \text{M}_\odot, M_{\text{WD,i}} = 0.5 \text{M}_\odot$, and $P_{\text{orb,i}} = 0.5$ days. The left panels display the evolution of the mass transfer rate (black solid line) and the orbital period (blue solid line). The right panels depict the evolution of the AML rate caused by GR (black solid line), the CAML rate (due to isotropic wind and FAML; red solid line), and the ratio of the CAML rate to the AML rate due to GR. The top panels correspond to the case without FAML. In the other three panels, from top to bottom, the values of $\nu_{\text{exp}}$ are taken to be $40, 80$, and $200 \text{ km s}^{-1}$, respectively.

In the left panels of Figure 1, we show that, due to the relatively large initial $q$, the system experiences a short thermal-timescale mass transfer phase during which growth of the WD mass occurs, and when FAML starts to work, the mass transfer evolves discontinuously. The reason is that the amplified mass transfer...
causes the orbital period to increase, leading to temporary RL detachment. This effect gradually declines when \( v_{\text{exp}} \) increases from 40 to 200 km s\(^{-1}\). In the right panels, variation in the mass transfer rate causes \( j_{\text{CAML}}/j_{\text{GR}} \) to vary between very small (\(<1\)) and large (\(>10^3\)) values. However, when the system has evolved across the period gap, the mass transfer rate decreases to low values (\(<10^{-10} M_\odot \text{yr}^{-1}\)), and GR begins to dominate the evolution. We find that the CAML rate decreases with time and is considerably less than \( j_{\text{GR}} \) during this stage. The FAML effect becomes weaker with increasing \( v_{\text{exp}} \). When \( v_{\text{exp}} = 200 \text{ km s}^{-1} \), the evolution below the period gap is very close to that without FAML.

In Figures 2 and 3, the initial WD masses are taken to be \( M_{\text{WD,1}} = 0.8 M_\odot \) and 1.1 \( M_\odot \), respectively. Due to the relatively small \( q \) value, the mass transfer rate has no chance to exceed \( \sim 3 \times 10^{-8} M_\odot \text{yr}^{-1} \), and nova eruptions prevent the mass growth of the WDs. In the case of FAML, the mass transfer rate is enhanced by several times for \( v_{\text{exp}} = 40 \text{ km s}^{-1} \) compared with the case of no FAML, but it still cannot enter the steady hydrogen-burning regime. The values of \( j_{\text{CAML}}/j_{\text{GR}} \) are similar for a given \( v_{\text{exp}} \) and all are significantly less than unity.

### 4. Discussion

In the previous section, we examined whether FAML can solve the extra 1.47\( j_{\text{GR}} \) AML problem for CVs below the period gap by calculating the secular evolution of CVs. In this section, we first attempt to derive a possible constraint on the extra AML mechanism in an analytical way. For the standard evolution of CVs, we assume that all of the accreted mass is lost from the binary during nova eruptions, taking away the specific AM of the WD. We can obtain the mass transfer rate as follows (Rappaport et al. 1983):

\[
\frac{M_2}{M_2} = \frac{1}{2} \left( \frac{R_2}{R_2} \right)_{\text{ev,th}} - \left( \frac{3(\zeta + q)}{2} \right)
\]

where \((R_2/R_2)_{\text{ev,th}}\) denotes the change in the donor star’s radius due to thermal or nuclear evolution, \(J_{\text{sys}}\) is the systematic AML rate, and \(\zeta\) is the adiabatic mass–radius exponent of the donor, namely \(R_2 \propto M_2^{\zeta}\). For low-mass main-sequence stars, the change in the stellar radius due to evolution can be ignored, i.e., \((R_2/R_2)_{\text{ev,th}} \approx 0\). For CVs below the period gap, let \(J_{\text{sys}} = 2.47J_{\text{GR}}\). Equation (6) can then be rewritten to be

\[
\frac{M_2}{M_2} = \frac{3}{6} + \frac{q}{2} - \frac{q}{3(1 + q)} - \frac{q^2}{1 + q},
\]

where

\[
M_2 = \frac{2.47J_{\text{GR}}}{J}
\]
From Equation (2), we have

$$ \dot{J}_{\text{CAML}} = \frac{(q + \nu_{\text{FAML}}) M_2 M_3}{M M_2}. $$

(8)

Letting $\dot{J}_{\text{CAML}} = 1.47 \dot{J}_{\text{GR}}$, we obtain

$$ \frac{1.47 \dot{J}_{\text{GR}}}{J} = \frac{(q + \nu_{\text{FAML}}) M_2 M_3}{M M_2}. $$

(9)

Combining Equations (2), (3), (7), and (9), and using the empirical formula for the RL radius (Schenker et al. 1998),

$$ R_{\text{L,2}} = \frac{8q}{81(1 + q)} \frac{1}{3}, $$

(10)

we finally get

$$ x = \frac{(0.496 + 0.297 \zeta) - q(1.47 + 3q)}{2.47 \times 3(1 + q)}, $$

(11)

where $x = \nu_{\text{rel}}/\nu_{\text{exp}}$. Equation (11) presents the required relation between $x$ and $q$ if FAML can account for the extra $1.47 \dot{J}_{\text{GR}}$ AML below the period gap. It is shown in Figure 4 with the black solid line based on the fit of the calculations for $M_{\text{W,D,1}} = 0.6 M_\odot$, $P_{\text{orb,1}} = 0.5$ days, and $\zeta \simeq 0.6$ (Liu & Li 2016). In comparison, we also plot the calculated $x$ as a function of $q$ during the evolution of CVs. The red, blue, and purple lines correspond to $M_{\text{W,D,1}} = 0.5$, 0.8, and 1.1 $M_\odot$, and the solid and dotted lines correspond to $\nu_{\text{exp}} = 40$ and 200 km s$^{-1}$, respectively. Obviously, the calculated $x$ is much smaller than required, implying that the adopted values of $\nu_{\text{exp}}$ are still too high.

In general, the expanding velocity of the ejected envelope for classical novae may exceed 1000 km s$^{-1}$ (Bode & Evans 2008). Yaron et al. (2005) showed that the mean expanding velocity of the ejected envelope is related to the mass and core temperature of the WDs and the mass transfer rate, ranging from less than 100 km s$^{-1}$ to over 3000 km s$^{-1}$ if the mass transfer rate $\gtrsim 10^{-12} M_\odot$ yr$^{-1}$. Their simulations also indicate that the expanding velocities are inversely correlated with the WD masses. Thus, the adopted values of $\nu_{\text{exp}}$ in our calculations actually underestimate $\nu_{\text{exp}}$. So, we conclude that the FAML mechanism seems unable to explain the extra AML below the period gap for CVs.

We then discuss the caveats and uncertainties in our work. Schreiber et al. (2016) assumed that triggering dynamically unstable mass transfer in CVs with low-mass WDs may be the result of a slow nova resembling a common-envelope phase. Although the nova eruptions are discontinuous events, our adoption of the long-term continuous wind interaction may not exactly reflect their real influence on the binary evolution. In addition, the drag force for the Bondi–Hoyle accretion in the

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### Table 3

| $M_2$ ($M_\odot$) | $M_{\text{W,D,1}}$ ($M_\odot$) | $M_{\text{W,D,2}}$ ($M_\odot$) | $P_{\text{orb,1}}$ (days) | $P_{\text{orb,2}}$ (minutes) | $\nu_{\text{exp}}$ (km s$^{-1}$) |
|------------------|-------------------------------|-------------------------------|---------------------------|-----------------------------|-----------------------------|
| 0.4              | 0.5                           | 0.5024                        | 0.316                     | 68.20                       | 80                          |
| 0.4              | 0.5                           | 0.5023                        | 0.501                     | 68.17                       | 80                          |
| 0.4              | 0.5                           | 0.5021                        | 0.794                     | 68.07                       | 80                          |
| 0.5              | 0.5                           | 0.5461                        | 0.316                     | 68.48                       | 80                          |
| 0.5              | 0.5                           | 0.5464                        | 0.501                     | 68.46                       | 80                          |
| 0.5              | 0.5                           | 0.5472                        | 0.794                     | 68.38                       | 80                          |

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### Table 4

| $M_2$ ($M_\odot$) | $M_{\text{W,D,1}}$ ($M_\odot$) | $M_{\text{W,D,2}}$ ($M_\odot$) | $P_{\text{orb,1}}$ (days) | $P_{\text{orb,2}}$ (minutes) | $\nu_{\text{exp}}$ (km s$^{-1}$) |
|------------------|-------------------------------|-------------------------------|---------------------------|-----------------------------|-----------------------------|
| 0.4              | 0.5                           | 0.5006                        | 0.316                     | 67.82                       | 200                         |
| 0.4              | 0.5                           | 0.5006                        | 0.501                     | 67.79                       | 200                         |
| 0.4              | 0.5                           | 0.5005                        | 0.794                     | 67.68                       | 200                         |
| 0.5              | 0.5                           | 0.5465                        | 0.316                     | 68.11                       | 200                         |
| 0.5              | 0.5                           | 0.5471                        | 0.501                     | 68.09                       | 200                         |
| 0.5              | 0.5                           | 0.5478                        | 0.794                     | 68.02                       | 200                         |

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The Calculated Results for the Evolution of CVs for $\nu_{\text{exp}} = 80$ km s$^{-1}$
Figure 1. Evolutionary tracks of a CV with $M_{2,i} = 0.6 \ M_\odot$, $M_{WD,i} = 0.5 \ M_\odot$, and $P_{\text{orb},i} = 0.5$ days. The top panels show the traditional CV evolution. In the other panels, FAML is included with $v_{\text{exp}} =$ 40, 80, and 200 km s$^{-1}$ from top to bottom. In the left panels, the black and blue lines represent the evolution of the mass transfer rate and the orbital period. In the right panels, the black, red, and blue lines denote the AML rate due to GR, the CAML rate, and the ratio of the AML rates due to CAML and GR, respectively.
common envelope is subject to substantial uncertainties. There is a dimensional parameter $c_{\text{drag}}$ in its expression (Equation (31) in Schenker et al. 1998) with its default value set to be 2. However, Kley et al. (1995) pointed out that radiation pressure may reduce $c_{\text{drag}}$ by a factor of 20. In Table 5, we present the calculated results by setting this parameter to 0.4 and 0.1 with $v_{\exp} = 40 \text{ km s}^{-1}$, denoted cases A and B, respectively. For both cases, we find that all results

![Figure 2. Same as Figure 1, but with $M_{\text{L}} = 0.6 M_\odot$, $M_{\text{WD}} = 0.8 M_\odot$, and $P_{\text{orb}} = 0.5 \text{ days}$.

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are quite similar to those in Tables 1 and 3, suggesting that the overall effect of FAML compared with that of GR is considerably small.

It should also be mentioned that the predicted minimum orbital periods (around 65–70 minutes) of CVs are substantially shorter than the observed ones (around 75–80 minutes). These
structures, thus leading the mass models, which affects the evolutionary time of the donor results are possibly related to the inadequacy of the AML models, which affects the evolutionary time of the donor structures, thus leading the mass--radius relation to reverse earlier or later. Setting the MB- and GR-induced AML rates to be 0.66 and 2.47 times the standard values above and below the period gap respectively, we recalculate the CV evolution and present the results in Table 5, denoted as case C. We find that the calculated minimum orbital periods are in accordance with the observed distribution. This further suggests that the effect of FAML on the orbital period evolution is very limited.

5. Conclusions

We summarize our results as follows:

1. FAML in the form of continuous wind interaction seems unable to account for the extra AML, apart from that due to GR, below the period gap for CVs, except when the nova envelope has extremely low expanding velocities.

2. FAML has a very limited influence on the minimum orbital period distribution of CVs.

Our results imply that there should be a more efficient mechanism that plays a role in CV evolution. The potential candidates could be residual MB and a CB disk. Thus, infrared observations of CVs will be crucial in testing the latter idea.

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Table 5
Examples of CV Evolution in Various Cases

| $M_2$ ($M_\odot$) | $M_{\text{WD},f}$ ($M_\odot$) | $M_{\text{WD},f}$ ($M_\odot$) | $P_{\text{orb},\text{min}}$ (days) | $P_{\text{orb},\text{min}}$ (minutes) | $v_{\text{exp}}$ (km s$^{-1}$) | Case |
|-----------------|-----------------|-----------------|-----------------|-----------------|-----------------|-----|
| 0.6             | 0.5             | 0.5376          | 0.316           | 68.05           | 40              | A   |
| 0.6             | 0.5             | 0.5387          | 0.501           | 68.04           | 40              | A   |
| 0.6             | 0.5             | 0.5385          | 0.794           | 67.99           | 40              | A   |
| 0.6             | 0.8             | 0.8             | 0.316           | 69.40           | 40              | A   |
| 0.6             | 0.8             | 0.8             | 0.501           | 69.37           | 40              | A   |
| 0.6             | 0.8             | 0.8             | 1.0             | 69.17           | 40              | A   |
| 0.6             | 1.1             | 1.1             | 0.316           | 70.55           | 40              | A   |
| 0.6             | 1.1             | 1.1             | 0.501           | 70.53           | 40              | A   |
| 0.6             | 1.1             | 1.1             | 1.0             | 70.13           | 40              | A   |
| 0.6             | 0.5             | 0.5377          | 0.316           | 67.87           | 40              | B   |
| 0.6             | 0.5             | 0.5354          | 0.501           | 67.84           | 40              | B   |
| 0.6             | 0.5             | 0.5358          | 0.794           | 67.78           | 40              | B   |
| 0.6             | 0.8             | 0.8             | 0.316           | 69.23           | 40              | B   |
| 0.6             | 0.8             | 0.8             | 0.501           | 69.21           | 40              | B   |
| 0.6             | 0.8             | 0.8             | 1.0             | 69.01           | 40              | B   |
| 0.6             | 1.1             | 1.1             | 0.316           | 70.40           | 40              | B   |
| 0.6             | 1.1             | 1.1             | 0.501           | 70.38           | 40              | B   |
| 0.6             | 1.1             | 1.1             | 1.0             | 70.11           | 40              | B   |
| 0.6             | 0.5             | 0.5386          | 0.501           | 74.63           | N/A             | C   |
| 0.6             | 0.8             | 0.8             | 0.501           | 76.56           | N/A             | C   |
| 0.6             | 1.1             | 1.1             | 0.501           | 78.22           | N/A             | C   |

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