NONTHERMALLY DOMINATED ELECTRON ACCELERATION DURING MAGNETIC RECONNECTION IN A LOW-$\beta$ PLASMA

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ABSTRACT

By means of fully kinetic simulations, we investigate electron acceleration during magnetic reconnection in a nonrelativistic proton–electron plasma with conditions similar to solar corona and flares. We demonstrate that reconnection leads to a nonthermally dominated electron acceleration with a power-law energy distribution in the nonrelativistic low-$\beta$ regime but not in the high-$\beta$ regime, where $\beta$ is the ratio of the plasma thermal pressure and the magnetic pressure. The accelerated electrons contain most of the dissipated magnetic energy in the low-$\beta$ regime. A guiding-center current description is used to reveal the role of electron drift motions during the bulk nonthermal energization. We find that the main acceleration mechanism is a Fermi-type acceleration accomplished by the particle curvature drift motion along the electric field induced by the reconnection outflows. Although the acceleration mechanism is similar for different plasma $\beta$, low-$\beta$ reconnection drives fast acceleration on Alfvénic timescales and develops power laws out of thermal distribution. The nonthermally dominated acceleration resulting from magnetic reconnection in low-$\beta$ plasma may have strong implications for the highly efficient electron acceleration in solar flares and other astrophysical systems.

Key words: acceleration of particles – magnetic reconnection – Sun: corona – Sun: flares

1. INTRODUCTION

Magnetic reconnection is a fundamental plasma process during which the magnetic field restructures itself and converts its energy into plasma kinetic energies (e.g., Priest & Forbes 2000). It occurs ubiquitously in laboratory, space, and astrophysical magnetized plasmas. An important unsolved problem is the acceleration of nonthermal particles in the reconnection region. Magnetic reconnection has been suggested as a primary mechanism for accelerating nonthermal particles in solar flares (Masuda et al. 1994; Krucker et al. 2010; Lin 2011), Earth’s magnetosphere (Oieroset et al. 2002; Fu et al. 2011; Huang et al. 2012), the sawtooth crash of tokamaks (Savrukhin 2001), and high-energy astrophysical systems (Colgate et al. 2001; Zhang & Yan 2011). In particular, observations of solar flares have revealed an efficient particle energization with 10%–50% of magnetic energy converted into energetic electrons and ions (Lin & Hudson 1976). The energetic particles usually develop a power-law energy distribution that contains energy on the same order of the dissipated magnetic energy (Krucker et al. 2010; Oka et al. 2015). Some observations find that the emission has no distinguishable thermal component, indicating that most of the electrons are accelerated to nonthermal energies (Krucker et al. 2010; Krucker & Battaglia 2014). This efficient production of energetic particles poses a challenge to current theories of particle acceleration.

Particle acceleration associated with reconnection has been studied in reconnection-driven turbulence (Miller et al. 1996), at shocks in the outflow region (Tsuneta & Naito 1998; Guo & Giacalone 2012), and in the reconnection layer (Drake et al. 2006; Fu et al. 2006; Oka et al. 2010; Kowal et al. 2012; Guo et al. 2014; Zank et al. 2014). Previous kinetic simulations have examined various acceleration mechanisms during reconnection, including the Fermi-type mechanism in magnetic islands (flux ropes in three-dimensional simulations; Drake et al. 2006; Guo et al. 2014) and direct acceleration in the diffusion region (Pritchett 2006; Huang et al. 2010). Most simulations focus on regimes with plasma $\beta \gtrsim 0.1$ with no obvious power-law distributions observed. It was argued that particle loss from the simulation domain is important for developing a power-law distribution (Drake et al. 2010). Early simulations of relativistic reconnection showed power-law distributions within the X-region (Zenitani & Hoshino 2001). Recent kinetic simulations with a highly magnetized ($\sigma = \frac{B^2}{4\pi n_i m_e c^2} \gg 1$) pair plasma found global power-law distributions without the particle loss, although the loss mechanism may be important in determining the spectral index (Guo et al. 2014, 2015). It is unknown whether or not this is valid for reconnection in a nonrelativistic proton–electron plasma since its property is different from the relativistic reconnection (Liu et al. 2015).

Motivated by the results of relativistic reconnection, here, we report fully kinetic simulations of magnetic reconnection in a nonrelativistic proton–electron plasma with a range of electron and ion $\beta_e = \beta_i = 0.007$–0.2. The low-$\beta$ regime was previously relatively unexplored due to various numerical challenges. We find that reconnection in the low-$\beta$ regime drives efficient energy conversion and accelerates electrons into a power-law distribution $f(E) \sim E^{-\gamma}$. At the end of the low-$\beta$ cases, more than half of the electrons in number and 90% in energy are in the nonthermal electron population. This strong energy conversion and particle acceleration led to a post-reconnection region with the kinetic energy of energetic particles comparable to magnetic energy. Since most electrons are magnetized in the low-$\beta$ plasma, we use a guiding-center drift description to demonstrate that the main acceleration process is a Fermi-type mechanism through the particle curvature drift motion along the electric field induced by fast plasma flows. The development of power-law distributions is consistent with the analytical model (Guo et al. 2014). The nonthermally
dominated energization may help explain the efficient electron acceleration in the low-β plasma environments, such as solar flares and other astrophysical reconnection sites.

In Section 2, we describe the numerical simulations. In Section 3, we present simulation results and discuss the conditions for the development of power-law distributions. We discuss and conclude the results in Section 4.

2. NUMERICAL SIMULATIONS

The kinetic simulations are carried out using the VPIC code (Bowers et al. 2008), which solves Maxwell’s equations and follows particles in a fully relativistic manner. The initial condition is a force-free current sheet with a magnetic field \( B = B_0 \tanh(z/\lambda) \hat{x} + B_0 \text{sech}(z/\lambda) \hat{y} \), where \( \lambda = d_i \) is the half thickness of the layer. Here, \( d_i \) is the ion inertial length. The plasma consists of protons and electrons with a mass ratio \( m_i/m_e = 25 \). The initial distributions for both electrons and protons are Maxwellian with uniform density \( n_0 \) and temperature \( kT_e = kT_i = 0.01m_e c^2 \). A drift velocity for electrons \( U_e \) is added to represent the current density that satisfies Ampere’s law. The initial electron and ion drift velocities \( \beta_e = \beta_i = 8 \pi n_0 k T_e / B_0^2 \) are varied by changing \( \omega_{pe}/\Omega_{ce} \), where \( \omega_{pe} = \sqrt{4 \pi n_0 e^2 / m_e} \) is the electron plasma frequency and \( \Omega_{ce} = e B_0 / (m_e c) \) is the electron gyrofrequency. Quantities \( \varepsilon_e = 0.007, 0.02, 0.06, \) and \( 0.2 \) correspond to \( \omega_{pe}/\Omega_{ce} = 0.6, 1, \sqrt{3} \) and \( 10 \), respectively. The domain sizes are \( L_x \times L_z = 200d_i \times 100d_i \). We use \( N_x \times N_z = 4096 \times 2048 \) cells with 200 particles per species per cell. The boundary conditions are periodic along the \( z \)-direction, perfectly conducting boundaries for fields and reflecting boundaries for particles along the \( z \)-direction. A long wavelength perturbation is added to induce reconnection (Birn et al. 2001).

3. SIMULATION RESULTS

Under the influence of the initial perturbation, the current sheet quickly thins down to a thickness of \(~d_i\) (electron inertial length \( c/\omega_{pe} \)) that is unstable to the secondary tearing instability (Daughton et al. 2009; Liu et al. 2013b). Figures 1(a) and (b) show the evolution of the out-of-plane current density. The reconnection layer breaks and generates a chain of magnetic islands that interact and coalesce with each other. The largest island eventually grows comparable to the system size and the reconnection saturates at \( t \Omega_{ci} \sim 800 \). Figure 1(c) shows the time evolution of the magnetic energy in the \( x \)-direction (the reconnecting component) \( \varepsilon_{bx} \) and the kinetic energy of electrons \( K_e \) and ions \( K_i \) for the case with \( \beta_e = 0.02 \), respectively. Throughout the simulation, 40% of the initial \( \varepsilon_{bx} \) is converted into plasma kinetic energy. Of the converted energy, 38% goes into electrons and 62% goes into ions. We have carried out simulations with larger domains (not shown) to confirm that the energy conversion is still efficient and weakly depends on system size. Since the free magnetic energy overwhelms the initial kinetic energy, particles in the reconnection region are strongly energized. Eventually, \( K_e \) and \( K_i \) are 5.8 and 9.4 times their initial values, respectively. Figure 1(d) shows the ratio of the electron energy gain \( \Delta K_e / K_e(0) \) for different cases. While the \( \beta_e = 0.2 \) case shows only mild energization, cases with lower \( \beta_e \) give stronger energization as the free energy increases.

The energy conversion drives strong nonthermal electron acceleration. Figure 2(a) shows the final electron energy spectra over the whole simulation domain for the four cases. More electrons are accelerated to high energies for lower-\( \beta_e \) cases, similar to earlier simulations (Bessho & Bhattacharjee 2010). More interestingly, in the cases with \( \beta_e = 0.02 \) and \( 0.007 \), the nonthermal energy spectra develop a power-law-like tail \( \varepsilon_{bt}(E) \sim E^{-p} \) with the spectral index \( p \sim 1 \). This is similar to results from relativistic simulations (Guo et al. 2014, 2015). We have carried out one simulation with \( m_i/m_e = 100 \) and \( \beta_e = 0.02 \) and find a similar electron spectrum. In contrast, the case with \( \beta_e = 0.2 \) does not show any obvious power-law tail, consistent with earlier simulations (Drake et al. 2010). The nonthermal population dominates the distribution in the low-\( \beta_e \) cases. For example, when we subtract the thermal population by fitting the low-energy distribution as Maxwellian, the nonthermal tail in the \( \beta_e = 0.02 \) case contains 55% of the electrons and 92% of the total electron energy. The power-law tail breaks at energy \( E_b \sim 10E_{th} \) for \( \beta_e = 0.02 \) and extends to a higher energy for \( \beta_e = 0.007 \). Figure 2(b) shows the fraction of nonthermal electrons for different cases. For \( \beta_e = 0.007 \), the nonthermal fraction goes up to 66%, but it decreases to 17% for \( \beta_e = 0.2 \). Figures 2(c) and (d) show \( n_{acc}/n_e \) at \( t \Omega_{ci} = 125 \) and 400 for the case with \( \beta_e = 0.02 \), where \( n_{acc} \) is the number density of accelerated electrons with energies larger than three times their initial thermal energy, and \( n_e \) is the total electron number density. The fraction of energetic electrons is over 40% and up to 80% inside the magnetic islands and reconnection exhausts, indicating a bulk energization for most of electrons in the reconnection layer. The energetic electrons will eventually be trapped inside the largest magnetic island. The nonthermally dominated distribution contains most of the converted magnetic energy, indicating that energy conversion and particle acceleration are intimately related.

To study the energy conversion, Figure 3(a) shows the energy conversion rate \( d \varepsilon_e / dt \) from the magnetic field to electrons through directions parallel and perpendicular to the
local magnetic field. We define \( d\varepsilon_e/ dt = \int_D j' \cdot E dV \), where \( D \) simulates the evolution of the electron energy. The electron energy \( E \) is normalized to the initial electron temperature \( E_{\text{th}} \). The black dashed line is the initial thermal distribution. The fraction of nonthermal electrons for different initial \( \beta_e \). \( n_{\text{non}}/n_0 \) is the number of nonthermal electrons obtained by subtracting the fitted thermal population from the whole particle distribution. The fraction of electrons with energies larger than three times the initial thermal energy at (c) \( \Omega_{\text{ci}} = 125 \) and (d) \( \Omega_{\text{ci}} = 400 \).

Figure 2. (a) Electron energy spectra \( f(E) \) at \( \Omega_{\text{ci}} = 800 \) for different \( \beta_e \). The electron energy \( E \) is normalized to the initial thermal energy \( E_{\text{th}} \). The black dashed line is the initial thermal distribution. (b) Time evolution of the fraction of nonthermal electrons for different initial \( \beta_e \). \( n_{\text{non}}/n_0 \) is the number of nonthermal electrons obtained by subtracting the fitted thermal population from the whole particle distribution. The fraction of electrons with energies larger than three times the initial thermal energy at (c) \( \Omega_{\text{ci}} = 125 \) and (d) \( \Omega_{\text{ci}} = 400 \).

By ensemble averaging the particle gyromotion and drift motions, the perpendicular current density for a single species can be expressed as (Parker 1957; Blandford et al. 2014)

\[
\mathbf{j}_\perp = P \frac{\mathbf{B} \times (\mathbf{B} \cdot \nabla) \mathbf{B}}{B^4} + P_1 \frac{\mathbf{B} \times \nabla \mathbf{B}}{B^2} + \rho m \frac{\mathbf{B}}{B^2} \times \frac{d\mathbf{E}}{dt}
\]

(1)

using a gyroscopic pressure tensor \( \mathcal{P} = P_1 \mathbf{I} + (P_1 - P_0) \mathbf{b} \mathbf{b} \), where \( P_1 \) and \( P_0 \) are the two pressure eigenvalues associated with eigenvectors perpendicular to the mean magnetic field direction (Scudder & Daughton 2008). \( A^\Omega \) measures the departure of the pressure tensor from cylindrical symmetry about the local magnetic field. It is zero when the local particle distribution is gyrotropic. Figure 3(b) shows that the regions with nonzero \( A^\Omega \) are localized to X-points. The small \( A^\Omega \) indicates that the electron distributions are nearly gyrotropic in most regions. Therefore, the drift description is a good approximation for electrons in our simulations even without an external guide field, which is required for this description in a high-\( \beta \) plasma (Dahlin et al. 2014).

Figures 4(a) and (b) show time-dependent \( d\varepsilon_e/ dt \) and \( \varepsilon_e \) from different current terms, where \( \varepsilon_e = \int_0^t (d\varepsilon_e/ dt) dt \). The contribution from polarization current and parallel current are small and not shown. The curvature drift term is a globally dominant term of \( \mathbf{j}_\perp \cdot \mathbf{E} \), the \( \nabla \mathbf{B} \) term gives a net cooling, and the magnetization term is small compared to these two. Figure 4(c) shows the spatial distribution of \( \mathbf{j}_\perp \cdot \mathbf{E} \). When the flow velocity \( \mathbf{u} \) is along the magnetic field curvature \( \kappa \) due to

Figure 3. (a) Energy conversion rate \( d\varepsilon_e/ dt \) for electrons through the parallel and perpendicular directions with respect to the local magnetic field, compared with the energy change rate of electrons \( dK_e/ dt \) for the case with \( \beta_e = 0.02 \). The shown values are integrals over the whole simulation domain. (b) Electron pressure agyrotropy \( A^\Omega \) at \( \Omega_{\text{ci}} = 400 \) in the same case. See the text for details.
It has been shown that the curvature drift acceleration in the reconnection region corresponds to a Fermi-type mechanism (Dahlin et al. 2014; Guo et al. 2014, 2015). To develop a power-law energy distribution for the Fermi acceleration mechanism, the characteristic acceleration time \( \tau_{\text{acc}} = 1/\alpha \) needs to be smaller than the particle injection time \( \tau_{\text{inj}} \) (Guo et al. 2014, 2015), where \( \alpha = (1/\varepsilon)(\partial \varepsilon/\partial t) \), and \( \partial \varepsilon/\partial t \) is the energy change rate of particles. To estimate the ordering of acceleration rate from the single-particle drift motion, consider the curvature drift velocity \( \nu = v_B^2 \times B / (\Omega_\text{e} B) \) in a curved field where \( R_e = |\kappa|^{-1} \), so the time for a particle to cross this region is \( \sim R_e/\nu \) and the electric field is mostly induced by the Alfvénic plasma flow \( \vec{E} \sim -\vec{v}_A \times \vec{B}/c \). The energy gain in one cycle is \( \delta \varepsilon \sim m_{\text{e}} \nu \varepsilon \). The time for a particle to cross the island is \( L_{\text{island}}/\nu \varepsilon \). Then, the acceleration rate \( \partial \varepsilon/\partial t \sim \varepsilon \nu \varepsilon /L_{\text{island}} \) for a nearly isotropic distribution. The characteristic acceleration time \( \tau_{\text{acc}} \sim L_{\text{island}}/\nu \varepsilon \). Taking \( L_{\text{island}} \sim 50d_0 \) and \( v_A \sim 0.2c \), the actual acceleration time \( \tau_{\text{acc}} \sim 250 \Omega_\text{e}^{-1} \). The actual acceleration time may be longer because the outflow speed will decrease from \( v_A \) away from the X-points, and the \( \nabla B \) term gives a non-negligible cooling effect. Our analysis has also found that preacceleration and trapping effects at the X-line region can lead to more efficient electron acceleration by the Fermi mechanism and are worthwhile to investigate further (Hoshino 2005; Egedal et al. 2015; Huang et al. 2015). Taking the main energy release phase as the injection time \( \tau_{\text{inj}} \sim 800 \Omega_\text{e}^{-1} \), the estimated value of \( \tau_{\text{inj}}/\tau_{\text{acc}} \sim 3.2 \), well above the threshold. For the case with \( \beta_e = 0.2 \), the ratio \( \tau_{\text{inj}}/\tau_{\text{acc}} \sim 0.32 < 1 \), so there is no power-law energy distribution.

4. DISCUSSION AND CONCLUSION

Nonthermal power-law distributions have rarely been found in previous kinetic simulations of nonrelativistic magnetic reconnection (Drake et al. 2010). We find that two essential conditions are required for producing power-law electron distribution. The first is that the domain should be large enough to sustain reconnection for a sufficient duration. A power-law tail develops as the acceleration accumulates long enough \( (\tau_{\text{inj}}/\tau_{\text{acc}} > 1) \). The second condition is that plasma \( \beta \) must be low to form a nonthermally dominated power-law distribution by providing enough free energy \((\sim 1/\beta)\) for nonthermal electrons. Assuming 10% of magnetic energy is converted into nonthermal electrons with spectral index \( p = 1 \), one can estimate that \( \beta_e \) is about 0.02 for half of the electrons to be accelerated into a power law that extends to \( 10E_\text{th} \). This agrees well with our simulation. We point out that a loss mechanism or radiation cooling can affect the final power-law index (Fermi 1949; Guo et al. 2014) of nonthermal electrons. Consequently, including loss mechanisms in a large three-dimensional open system is important, for example, to explain the observed power-law index in solar flares and other astrophysical processes. Another factor that may influence our results is the presence of an external guide field \( B_g \). Our preliminary analysis has shown that the Fermi acceleration dominates when \( B_g \lesssim B_0 \). The full discussion for the cases including the guide field will be reported in another publication (X. L. Li et al. 2015, in preparation). A potentially important issue is the three-dimensional instability, such as kink instability that may strongly influence the results. Unfortunately, the corresponding three-dimensional simulation is beyond the available computing resources. We note that results from three-dimensional simulations with pair plasmas have...
shown development of strong kink instability but appear to have no strong influence on particle acceleration (Guo et al. 2014; Sironi & Spitkovsky 2014). The growth rate of the kink instability can be much less than the tearing instability for a high mass ratio (Daughton 1999), and therefore the kink instability may be even less important for electron acceleration in a proton–electron plasma.

In our simulations, the low-β condition is achieved by increasing magnetic field strength (or equivalently decreasing density). We have carried out low-β simulations with the same magnetic field but lower temperature and found a similar power-law distribution (X. L. Li et al. 2015, in preparation).

The energy partition between electrons and protons shows that more magnetic energy is converted into protons. For simulations with a higher mass ratio $m_i/m_e = 100$, the energetic electrons still develop a power-law distribution, and the fraction of electron energy to the total plasma energy is about 33%, indicating that the energy conversion and electron acceleration are still efficient for higher mass ratios. Our results show that ions also develop a power-law energy spectrum for low-β cases and the curvature drift acceleration is the leading mechanism. However, the ion acceleration has a strong dependence on the mass ratio $m_i/m_e$ for our relatively small simulation domain ($\sim 100d_i$). We therefore defer the study of ion acceleration to a future work (X. L. Li et al., 2015, in preparation).

The energetic electrons can generate observable X-ray emissions. As nonthermal electrons are mostly concentrated inside the magnetic islands, the generated hard X-ray flux can be strong enough to be observed during solar flares in the above-the-loop-top region (Masuda et al. 1994; Krucker et al. 2010) and the reconnection outflow region (Liu et al. 2013a). The nonthermal electrons may also account for the X-ray flares in the accretion disk corona (Galeev et al. 1979; Haardt et al. 1994; Li & Miller 1997).

In summary, we find that in a nonrelativistic low-β proton–electron plasma magnetic reconnection is highly efficient at converting the free energy stored in a magnetic shear into plasma kinetic energy and accelerating electrons into nonthermal energies. The nonthermal electrons contain more than half of the total electrons, and their distribution resembles power-law energy spectra with spectral index $p \sim 1$ when particle loss is absent. This is in contrast to the high-β case, where no obvious power-law spectrum is observed. It is important to emphasize that the particle acceleration discussed here is distinct from the acceleration by shocks, where the nonthermal population contains only about 1% of particles (Neergaard Parker & Zank 2012).

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