Unitarity constraints on neutral pion electroproduction

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At large virtuality $Q^2$, the coupling to the vector meson production channels provides us with a natural explanation of the surprisingly large cross section of the neutral pion electroproduction recently measured at Jefferson Laboratory, without destroying the good agreement between the Regge pole model and the data at the real photon point. Elastic rescattering of the $\pi^0$ provides us with a way to explain why the node, that appears at $t \sim -0.5$ GeV$^2$ at the real photon point, disappears as soon as $Q^2$ differs from zero.

The electroproduction of neutral pion raises two issues. The first one is a long standing issue (mid 70s): the node that appears at $t \sim -0.5$ GeV$^2$ at the real photon point [1] disappears as soon as the virtuality of the photon $Q^2$ differs from zero [2]. Several attempts, ranging from Regge cuts [3–5] to direct coupling to quarks and rearrangement [6], were proposed to qualitatively explain this result. However, no quantitative explanation has been proposed yet, except at the expense of a strong variation with $Q^2$ of the elastic cut [7]. The second issue is more recent and was raised, about three years ago, during the preliminary analysis of the data obtained at Jefferson Laboratory (JLab) in HallA and in HallB. When extrapolated at large $Q^2$, any Regge pole model that leads to a fair understanding of the raw $Q^2$ data grossly underestimates the JLab data. The HallA data [8] have just been released; the HallB data [9] are still in the final stage of analysis and will be released soon.

In this Letter, I propose a solution of these two problems which combines elastic $\pi^0$ rescattering and the coupling to inelastic $\omega p, \rho^- n, \rho^- \Delta^0$ and $\rho^- \Delta^{++}$ channels. A recent measurement at JLab [10] has shown that the cross section of the $p(\gamma^*, \rho^-)n$ channel, which is very small at the real photon point, becomes comparable to, and even larger than, the cross section of the $p(\gamma^*, \rho^0)p$ channel, at large virtuality $Q^2$.

Fig. 1 summarizes these findings. The DESY data have been recorded in a geometry where the $\pi^0$ is emitted perpendicular to the electron scattering plane (azimuthal angle $\phi = 90^\circ$) that emphasizes the transverse component of the cross section. The JLab data have been integrated over the $\pi^0$ azimuthal angle and correspond to the combination of the transverse and longitudinal cross sections $d\sigma_T/dt + \epsilon d\sigma_L/dt$, where $\epsilon$ is the polarization of the virtual photon. The combination of the Regge pole and the $\pi^0$ elastic scattering amplitude (Pomeron cut) allows to reproduce the cross section at moderate $Q^2$ ($\sim 0.5$–1 GeV$^2$), but underestimates the JLab data at higher $Q^2$. The coupling to the charged $\rho$ production channels brings the theoretical cross section close to the JLab data at $Q^2 = 2.3$ GeV$^2$. It is remarkable, and was rather unexpected, that the cross section, at $-t \sim 0.3$, does not change between $Q^2 = 0.85$ and 2.3 GeV$^2$.

The basic Regge pole amplitudes are fully described in Ref. [11] (GLV). Instead of their expression in terms of $\gamma$ matrices, I use the expression of the $\omega$ and $\rho$ (that are given in the appendix of Ref. [12]), as well as the expression of the $b_1, t$-channel exchange amplitudes in terms of $\sigma$ matrices. In the GLV scheme, the node in the real photon cross section near $t = -0.5$ GeV$^2$ is naturally generated by the use of a non-degenerated amplitude of the $\omega$ Regge pole. The contribution of the $\rho$ Regge pole with a degenerated amplitude fills in the dip and brings the GLV model close to the data. The exchange of the $b_1$ meson does not contribute significantly to the unpolarized cross section, but is needed to account for the measured photon asymmetry $\Sigma$. Multiplying each amplitude by an electromagnetic form factor $F_M(Q^2)$ keeps the shape of the real photon cross section in the virtual photon sector, in contradiction with experiment.

The other way to generate a node in a Regge amplitude is to use a degenerated amplitude and supplement it by the elastic absorptive cut. Assuming that the elastic scattering amplitude is driven by the Pomeron exchange, it is possible to express the cut amplitude as an effective Regge pole [13]. In this scheme, the $\omega$ Regge exchange amplitude takes the form:
\[
\alpha_{\omega}(t) = \alpha_{\omega}(0) + \alpha'_{\omega} t = 0.44 + 0.9 t \\
\alpha_{\epsilon}(0) = \alpha_{\omega}(0) + \alpha_{\rho}(0) = 1 = 0.44, \\
\alpha_{\epsilon}' = (\alpha_{\omega}' + \alpha_{\rho}') / (\alpha_{\omega}' + \alpha_{\rho}) = 0.2
\]

where the intercept and the slope of the Pomeron Regge trajectory are respectively \( \alpha_{\rho}(0) = 1 \) and \( \alpha_{\rho}' = 0.25 

The purely destructive interference between the pole and the cut amplitudes is a direct consequence of the structure of the rescattering loop amplitude and the almost purely absorptive nature of the elastic \( \pi N \) scattering amplitude (see Eqs. (9) to (11) and the corresponding discussion in Ref. [14]). It is possible to reproduce the GLV non-degenerated \( \omega \) amplitude (squared) with the following choice (dotted line curve in Fig. 2):

\[
g_{\omega NN}^2/4\pi = 4.9, \\
G_c(t) = 3.7 e^{2t}.
\]

It is worth pointing out that the \( \omega NN \) coupling constant is about half of the GLV one (\( g_{\omega NN}^2/4\pi = 17.9 \)), in better agreement with the range of values that are determined in the analysis of low energy \( NN \) scattering data. It is also almost the same as the value \( (g_{\omega NN}^2/4\pi = 6.44) \) needed in the analysis of the \( p(\gamma, \eta) p \) reaction [16]. In this channel, there is no node and the \( \eta N \) scattering cross section is much lower than the \( \pi N \) one: The use of a degenerated \( \omega \) Regge amplitude alone, with no elastic cut, is more justified. The exchange of the \( \rho \) degenerated trajectory, with the same coupling constants as in GLV, brings the model close to the unpolarized cross section.

In the first version of this paper [17] an axial-vector \( b_1 NN \) coupling was used, as in the GLV scheme. It turns out that this coupling is forbidden: it is allowed at the \( a_1 NN \) vertex, but the \( a_1 \) meson does not couple to the neutral pion. Therefore, I use the following \( b_1 \) exchange current which is based on an axial-tensor \( b_1 NN \) coupling:

\[
\mathcal{J}^\mu_{b_1} = \frac{g_{b_1 NN}}{m_{b_1}} \frac{k_{b_1}}{2m} \bar{p}(p_f)\gamma_\mu u(p_i)(2p_f^{\mu}k_{b_1}-2p_i^{\mu}k_{b_1}) \\
\times e^{-i\pi \alpha_{\pi}(t)} \left( \frac{s}{s_0} \right)^{-1} \alpha_{\pi}'(1 - \alpha_{\pi}) F_{b_1}(Q^2)
\]

where the Regge trajectory is the same as the pion degenerated trajectory and the electromagnetic coupling constant \( g_{b_1 NN} \) is the
reproduces fairly well the experimental data [18] around the c.m. energy and even larger than the meant. The agreement is good too at $Q^2 = 0.55$ GeV$^2$, but it is not possible to get rid of the second maximum in $t$ when $Q^2 = 0.22$ GeV$^2$. Also, the extrapolation of this scheme at $Q^2 = 2.3$ GeV$^2$ misses the recent JLab data.

The first inelastic cut that may play a role is the Charge Exchange (CEX) pion rescattering cut (Fig. 3). The charged pion electroproduction [18], around $Q^2 = 2.3$ GeV$^2$, is larger ($\sim 3$ μb/GeV$^2$) than the π$^+$ one ($\sim 0.4$ μb/GeV$^2$) at low $t$. Neglecting its principal part, the corresponding rescattering matrix element reduces to [14]:

$$T_{\pi N} = -i \frac{p_{\pi}^\ast m}{16\pi^2} \int d\Omega \left[ T_{\pi^+ n \to \pi^+ n} (t_\pi) T_{\pi^+ n \to \pi^+ n} (t_\pi) \right]$$

where $p_{\pi}^\ast = \sqrt{(s - (m_\pi - m)^2)(s - (m_\pi + m)^2)/4s}$ is the on-shell momentum of the intermediate neutron, for the c.m. energy $\sqrt{s}$. The two fold integral runs over the solid angle $\Omega$ of the intermediate neutron, and is performed numerically. The four momentum transfer between the incoming photon and the intermediate $\pi$ is $t_\pi = (k_\pi - P_\pi)^2$, while the four momentum transfer between the intermediate and the outgoing pions is $t_\pi = (k_\pi - P_\pi)^2$. The summation over all the spin indices of the intermediate particles is meant.

For the $p(\gamma^*, \pi^+)n$ amplitude, I use the VGL model [19] which reproduces fairly well the experimental data [18] around $Q^2 = 2.3$ GeV$^2$ and $\sqrt{s} = 2.2$ GeV, at least the Longitudinal part. The expression of the CEX amplitude is:

$$T_{\text{CEX}} = \frac{3}{2} \frac{g_{\rho \pi} (1 + \kappa_V)}{m} \frac{1}{\sqrt{s}} g_{\rho \pi} T^{\rho}_{\rho_{\pi}} F_1(t_\rho) (\lambda_\rho | \vec{P}_{\rho} \times \vec{k}_\rho | \rho \rho)$$

where $g_{\rho \pi}^2/4\pi = 5.71$, where $g_{\rho}^2/4\pi = 0.92$, where $\kappa_V = 6$ and where $F_1$ is the nucleon form factor as defined in [14]. Since the experimental $t$ distribution exhibits a node, I use the non-degenerated Regge propagator $P^{\rho}_{\pi}$ with the saturating trajectory of the $\rho$ [11]. As shown in Fig. 4, this gives a good account of the $\pi N$ CEX scattering data [20] in the same energy range.

Since the $\pi N \Delta$ and $\rho N \Delta$ coupling constants are comparable to and even larger than the $\pi N N$ and the $\rho N N$ ones (see for instance Ref. [21]), the $\pi^+ \Delta^+$ and $\pi^- \Delta^{-}$ intermediate states play also a role (Fig. 3). The rescattering matrix element is a straightforward extension of Eqs. (6) and (7), using the relevant coupling constants as well as the relevant isospin coefficients, and replacing the $\vec{P}_\rho$ matrices by the $\Delta \rightarrow \Delta$ spin transition matrices $\vec{S}$.

Fig. 3. The charge exchange pion rescattering graphs.

$\gamma \to p(\pi^+)n$ cut alone

Fig. 4. The $\pi N$ CEX at $\sqrt{s} = 2.4$ GeV [20]. The (black) line, marked “lin”, corresponds to the use of a linear Regge trajectory, while the (red) line, marked “sat”, corresponds to the use of a saturating Regge trajectory. (For interpretation of the references to color in this figure legend, the reader is referred to the web version of this Letter.)

Fig. 5 shows that the coupling to these CEX channels is not enough to account for the large experimental cross section at $Q^2 = 2.3$ GeV.

The next cuts are the vector meson cuts shown in Fig. 6. The generic amplitude is:

$$T_{\rho \gamma} = -i \frac{p_{\rho \gamma} M}{16\pi^2} \int \frac{d\Omega}{\sqrt{s}} \left[ T_{\rho \gamma \rightarrow \gamma V} T_{V \Delta} \right]$$

where $p_{\rho \gamma} = \sqrt{(s - (m_\rho - M)^2)(s - (m_\gamma + M)^2)/4s}$ is the on-shell momentum of the intermediate baryon (of mass $M$), for the c.m. energy $\sqrt{s}$. The two fold integral runs over the solid angle $\Omega$ of the intermediate baryon. The four momentum transfer between the incoming photon and the vector meson is $t_\gamma = (k_\gamma - P_\gamma)^2$, while the four momentum transfer between the vector meson and the target proton is $t_\gamma = (k_\gamma - P_\gamma)^2$. The summing over all the spin indices of the intermediate particles is meant.

Fig. 5. The contribution of the $\pi N$ (dashed red line), the $\pi \Delta$ (full black line) CEX cuts and of the $\omega \rho$ cut (dash-dotted black line) to the cross section at $Q^2 = 2.3$ GeV$^2$ and $\sqrt{s} = 2.269$ GeV. The dotted blue line is the contribution of the Regge poles. The contribution of the $\pi N + \pi \Delta$ cuts alone is shown in the bottom of the figure. The dotted lines correspond to the longitudinal component only. (For interpretation of the references to color in this figure legend, the reader is referred to the web version of this Letter.)
the Regge trajectories of the Pomeron, the is larger than the cross section of the n channel and of the proton in the spin indices of the intermediate particles is meant. 

Fig. 6. The vector meson cuts.

Since the \( \rho^0 \) cannot decay into two \( \pi^0 \)'s, only the \( \omega \), the \( \rho^+n \) and the \( \rho^\pm \Delta \) cuts have to be taken into account. In the \( \omega p \) cut, the amplitude of the \( p(\gamma,\omega)p \) reaction is based on the exchange of the Regge trajectories of the Pomeron, the \( \pi \), the \( f_2 \) in the \( t \)-channel and of the proton in the \( u \)-channel. The model is described in Ref. [22] and reproduces well the experimental data [23] in the \( J\text{Lab} \) energy and momentum range. The amplitude of \( p(\omega,\pi^0)p \) has the same structure [12] as the \( \rho \) exchange part of the Regge amplitude of the reaction \( p(\gamma,\pi^0)p \), to which it is related under the Vector Meson Dominance assumption:

\[
T_{\omega\pi} = \frac{f_{\omega}}{\sqrt{4\pi}} \times T_{\gamma\pi}
\]

where \( f_{\omega}^2/4\pi = 18.4 \), and where the amplitude is evaluated with the actual kinematics of the \( p(\omega,\pi^0)p \) reaction. This model leads to a very good agreement with the available data (Fig. 7). Again, the contribution of the \( \omega p \) cut is not enough to reproduce the experimental data at \( Q^2 = 2.3 \text{ GeV}^2 \) (Fig. 5).

The contribution of the \( \rho^+n \) cut is far more important (Fig. 1). The first reason is that the cross section of the \( N(\rho,\pi)n \) reaction is larger than the cross section of the \( N(\omega,\pi)n \) reaction at low \( t \) (compare Fig. 3 of [14] and Fig. 7): The former reaction is driven by \( \pi \) exchange while the latter is driven by \( \rho \) exchange. The second reason is that the cross section of the \( p(\gamma,\rho^+)n \) arises at its real photon point, becomes large at large \( Q^2 \). This is shown in Fig. 8 which compares the cross sections of the \( p(\gamma,\rho^0)N \) and \( p(\gamma,\rho^+)n \) reactions at the real photon point and at \( Q^2 = 2.3 \text{ GeV}^2 \). The reference to the experimental cross sections of the \( \rho^0 \), as well as the description of the model, can be found in [22,25]. At the real photon point, the cross section of the \( n(\gamma,\rho^+)p \) reaction comes from [26]. At \( Q^2 = 2.3 \text{ GeV}^2 \), the two data of the \( p(\gamma,\rho^+)n \) reaction are preliminary and given for illustration only. They come from the preliminary analysis of a \( J\text{Lab} \) experiment [10]. The model of the \( p(\gamma,\rho^+)n \) reaction is based on the exchange of the \( \pi^+ \) and \( \rho^+ \) Regge trajectories. The \( \pi \) exchange amplitude is the same as the amplitude [22,25] that dominates the \( p(\gamma,\omega)p \) reaction (with trivial changes of the coupling constants).

It is not important and the dominant contribution comes from the \( \rho \) exchange amplitude. Its vector part takes the form:

\[
T_{\rho\rho^+} = \frac{e\rho_\ell(\kappa_V + 1)}{2m} \sqrt{2F_{\rho}}(Q^2, t)(t - m^2)P^\rho_{\ell} \\
\times \left( \lambda_f(2\tilde{P}_{\rho} - \vec{k}_f) \cdot \vec{\sigma} \cdot (\tilde{P}_{\rho} - \vec{k}_\rho) \times \vec{\sigma}_{\rho} \right) \\
\times \left( 2\tilde{P}_{\rho} + \vec{k}_\rho - \tilde{\sigma}_{\rho} \right) \cdot \vec{\sigma} \cdot \tilde{P}_{\rho} \times \tilde{\sigma}_{\rho} \\
\times \left( \vec{\sigma} \cdot \tilde{P}_{\rho} \times \tilde{\sigma}_{\rho} + \tilde{\sigma} \cdot \tilde{\sigma}_{\rho} + \lambda_f \right) \\
\times \sqrt{(E_i + m)(E_f + m)} \\
\times 2m
\]

Fig. 7. The cross section of the \( p(\pi^-,\omega)n \) reaction at \( \sqrt{s} = 2.785 \text{ GeV} \) [24].

Fig. 8. The comparison between the cross sections of the \( p(\gamma,\rho^0)p \) (black) and \( p(\gamma,\rho^+)n \) (red) reactions at \( Q^2 = 0 \) (top) and \( Q^2 = 2.3 \text{ GeV}^2 \) (bottom). The open red circles and the dash-dotted red curve correspond to the photo-production of \( \rho^+ \), while the filled red circles and the full red curves correspond to the electroproduction of \( \rho^+ \). (For interpretation of the references to color in this figure legend, the reader is referred to the web version of this Letter.)

Fig. 9. The graphs of the reaction \( p(\gamma,\rho^+)n \). Top: meson exchange graphs. Bottom: Contact and nucleon exchange gauge graphs.
constants are $g_s^2/4\pi = 0.4$ and $\kappa_V = 6$. One recognizes easily the $\rho$ pole term as well as the nucleon s-channel pole term and the contact term (see Fig. 9) that are necessary to make the amplitude gauge invariant.

I use the GLV degenerated Regge propagator $P^\rho_\circ$, with a linear trajectory, and the $t$ dependent electromagnetic form factor $F_\rho(Q^2, t)$ of [22] with a cut-off mass of $A_T^2 = 0.9$ GeV$^2$. Under those assumptions, the model not only predicts the right transverse and longitudinal integrated cross sections (Fig. 8) from the real photon point to large $Q^2$, but also their $t$ distribution in the whole range ($1.5 < Q^2 < 4$ GeV$^2$, $2 < \sqrt{s} < 2.8$ GeV) that has been covered in the JLab HallB experiment [10]. The model will be compared to the final JLab data in the experimental Letter.

As shown in Fig. 1, the contribution of the $\rho^+ n$ cut accounts for about half of the cross section at $Q^2 = 2.3$ GeV$^2$, modifies little the cross section at $Q^2 = 0.55$ and 0.85 GeV$^2$, but interferes with the Regge pole contribution at $Q^2 = 0.25$ GeV$^2$. At this point of the discussion it is worth to emphasize that no freedom is left in the amplitudes of the cuts, in that sense that the unitarity integral relates on-mass-shell elementary amplitudes of the production and absorption of the intermediate mesons. As soon as those amplitudes reproduce the elementary reaction cross sections, the amplitude of each cut is frozen and their relative contribution is driven by the actual relative size of the cross section of the elementary channels. So, this singular part of the rescattering integrals is on solid grounds and consistently relates several channels that have been studied recently at JLab or elsewhere: it simply cannot be overlooked.

The contribution of the principal part of the rescattering integrals is not so well constrained as it requires the knowledge of either the off-mass shell amplitudes, if is calculated by brute force, or their asymptotic behavior, if it is determined by a dispersion relation. This is an open issue, but I simply note that the measured ratio between the real part and the imaginary part of the amplitude does not exceed 10% in Compton scattering or meson–nucleon elastic scattering at forward angles. So there is good reason to expect that the principal part of the rescattering integrals contributes little.

The third reason why the coupling to the charged $p$ production channels is strong is that the contribution of the $\Delta$'s intermediate states (Fig. 6) is as important as the contribution of the neutron intermediate state. Since there are no measured cross sections of the $N(\gamma^*, p^+)\Delta$ reaction in the virtual photon sector, I note that, at lowest order, the structure of the lower part of the loop diagrams is very similar:

$$\vec{S} \cdot \vec{k}_\rho \cdot \vec{k}_\pi = \vec{k}_\rho \cdot \vec{k}_\pi + \alpha \vec{k}_\rho \times \vec{k}_\pi,$$

$$\vec{S}^\dagger \cdot \vec{k}_p \cdot \vec{k}_\pi = \frac{2}{3} \vec{k}_p \cdot \vec{k}_\pi + \frac{1}{3} \vec{S} \cdot \vec{k}_\rho \times \vec{k}_\pi$$

(11)

where $\vec{S}$ is the spin operator of the $N \to \Delta$ transition. Assuming that the scalar and vector parts contribute equally:

$$T_N + T_V + T_{A++} = T_N \left(1 + \frac{1}{2} \frac{p_{\Delta} m_{\Delta}}{p_m} \frac{G_p G_\pi}{G_\rho G_\pi} \left(1 + \frac{1}{2} \right) \right)$$

$$= T_N \left(1 + 1.5 \frac{p_{\Delta} m_{\Delta}}{p_m} \right)$$

(12)

where $p_{\Delta}$ and $p$ are the momenta of the $\Delta$ and the neutron in the $\rho \Delta$ and $p n$ loop respectively, and where the ratio of the coupling constant is $G_p G_\pi / G_\rho G_\pi = 4.49$ according to [21]. The last bracket contains the ratio of the isospin coefficients $1/2$ in the $A^{++}$ channel and $1/6$ in the $A^0$ channel. For the $\pi \Delta$ cuts, such an estimate is consistent with the numerical evaluation of the integral that is shown in the bottom part of Fig. 5. I also note that, at the real photon point, the same kind of estimate predicts a cross section of the $p(\gamma, \rho^+)\Delta^0$ reaction comparable to the cross section of the $p(\gamma, \rho^+)n$ reaction, in accord with the only experiment [27] available so far.

Under those assumptions, the model becomes close to the JLab HallB data at $Q^2 = 2.3$ GeV$^2$ (Fig. 1) without destroying the good agreement at the real photon point (Fig. 2). It slightly overestimates the DESY data at $Q^2 = 0.55$ and 0.85 GeV$^2$. This can be fixed by a fine tuning of the cut off masses in the electromagnetic form factors of the Regge poles, which I had chosen to reproduce the DESY data without the cut contribution. This will not affect the agreement at the lowest and the highest $Q^2$. However the model already gives a good account of the preliminary JLab HallB data [9] in the range $1.5 < Q^2 < 4$ GeV$^2$, $2 < \sqrt{s} < 2.8$ GeV, and I postpone such an adjustment until the final data are released.

Fig. 10 shows the comparison of the model with the response functions which have been determined at JLab for two values of $Q^2$. I use the following definition:

$$2\pi \frac{d\sigma}{dt} = \frac{d}{d\phi} \left[ \sigma_T + \sigma_L \right]$$

$$+ \epsilon \cos(2\phi) \sigma_{TT} + \sqrt{2\epsilon(\epsilon + 1)} \cos(\phi) \sigma_{TL} + h \sqrt{2\epsilon(1 - \epsilon)} \sin(\phi) \sigma_{LT}$$

(13)

and I have renormalized the experimental transverse–longitudinal cross sections [8], $\sigma_{TL}$ ad $\sigma_{LT}$, accordingly.

Besides the unpolarized cross section ($\sigma_T + \sigma_L$), the model reproduces also the transverse–transverse interference response function $\sigma_{TT}$. The understanding of the slow variation of the cross section is a non-trivial result. At the lowest $Q^2 = 1.94$ GeV$^2$, the mass of the intermediate state is $\sqrt{s} = 2.052$ GeV, slightly above the $\rho \Delta$ threshold (2.010 GeV). At fixed $X = 0.368$, $\sqrt{s}$ increases when $Q^2$ increases, and the onset of the $\rho \Delta$ cuts compensates the decrease with $Q^2$ and $\sqrt{s}$ of the Regge amplitudes that drive
Fig. 11. The beam asymmetry [28] recently measured at JLab, for $Q^2 = 2.3$ GeV$^2$, $X = 0.35$ ($\sqrt{s} = 2.27$ GeV) and $\phi = 90^\circ$. The dotted curve takes only into account the $\omega$, $\rho$ and $b_1$ Regge pole contributions. The dash-dotted curve includes also the CEX cuts contribution. The full curve includes all the cuts contributions.

Fig. 12. The target asymmetry [29] recently measured at JLab, for $Q^2 = 1.82$ GeV$^2$, $\sqrt{s} = 2.358$ GeV and $t = -0.31$ GeV$^2$. Dashed line: $\omega$ and $\rho$ poles. Dotted line: $b_1$ pole included. Dash-dotted line: $\pi$ CEX cuts included. Full line: Vector meson cuts included.

the loop amplitudes. The contribution of the cuts is small in $\sigma_{\Pi}$, but large in the transverse–longitudinal response functions $\sigma_{\Pi L}$ and $\sigma_{\Pi L}$. The model predicts the same sign and magnitude as the JLab HallA fifth response function $\sigma_{\Pi L}^\ast$ (polarized electrons), and therefore reproduces the beam asymmetry $A_{UL}$ (Fig. 11) that has been recorded in HallB [28]. But it predicts a different sign for the transverse–longitudinal response function $\sigma_{\Pi L}$. Since it predicts the same sign and magnitude as the preliminary HallB $\sigma_{\Pi L}$ [9], I leave open the discussion until the final data are released.

Finally, the unitarity cuts are also the key to the successful interpretation of the target asymmetry $A_{UL}$ (Fig. 12). The CEX cuts contribute, but falls short. The $\rho^-n$ and $\rho \Delta$ cuts lead to the right sign and the right magnitude of the signal.

In conclusion, the coupling to the vector meson production channels provides us with a natural explanation of the large cross section of the $\pi^0$ electroproduction cross section at $Q^2 \sim 3$ GeV$^2$. Only a few intermediate hadronic states contribute to the unitarity cuts, which are on solid grounds when the elementary production and absorption cross sections are large and are known. So far, we are still in the hadronic regime and we have not reached the domain of factorization between a hard perturbative scattering and a soft non-perturbative nucleon structure function.

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