Human Motion Prediction using Adaptable Neural Networks

Yujiao Cheng*, Weiye Zhao*, Changliu Liu, and Masayoshi Tomizuka

Abstract—Human motion prediction is an important component to facilitate human robot interaction. Robots need to accurately predict human’s future movement in order to efficiently collaborate with humans, as well as to safely plan its own motion trajectories. Many recent approaches predict human’s future movement using deep learning methods, such as recurrent neural networks. However, existing methods lack the ability to adapt to time-varying human behaviors. Moreover, many of them do not quantify uncertainties in the prediction. This paper proposes a new approach that uses an adaptable neural network for human motion prediction, in order to accommodate human’s time-varying behaviors and to provide uncertainty bounds of the predictions in real time. In particular, a neural network is trained offline to represent the human motion transition model. Recursive least square parameter adaptation algorithm (RLS-PAA) is adopted for online parameter adaptation of the neural network and for uncertainty estimation. Experiments on several human motion datasets verify that the proposed method outperforms the state-of-the-art approach with a significant improvement in terms of prediction accuracy and computation efficiency.

I. INTRODUCTION

Smooth interactions among intelligent entities depend on a clear understanding of what the others would do in various circumstances. For example, soccer players predict the motions of their teammates for better cooperation; pedestrians have a notion of where others are going so as to avoid collisions. Similarly, robots that interact in proximity with humans are required to be aware of what the human is going to do in the near future. The benefits are that, based on the predictions, robot can plan collision-free trajectories to assure human’s safety and that robots can plan and schedule their actions to improve task efficiency. Besides the applications in human robot interaction [1] [2] [3], human motion prediction also plays a key role in computer graphics (CG) [5], and psychology biological motion modeling [6].

However, human motion is inherently difficult to predict due to the nonlinearity and stochasticity in human behavior [7]. In addition, individual differences are also prominent. Prediction models that work for one person may not be applicable to another.

Early attempts have been made to predict human motion using kalman filter and particle filter [8] [9], where the problem is posed as a tracking problem. Another category of approaches assumes that human is rational with respect to certain cost functions. Human trajectories can then be predicted by optimizing the cost function [10]. The difficulty of this method is that the cost functions of human are hard to obtain due to stochasticity and complexity in human intention. Another domain of work prominently focuses on latent variable based probabilistic models. Wu et al. [11] use hidden markov models (HMMs) combined with multi-layer perceptrons to model the evolution patterns of motion trajectory.

Similar to HMMs, recurrent neural networks (RNNs) have distributed hidden states to store information about the past. But RNNs are more powerful for greater function capacity. Despite that many works on RNNs have obtained big success on human motion prediction [12] [13], they still suffer from several problems. First problem is that RNNs are hard to train. Heroic efforts of many years still fail to accelerate the training speed of RNNs. Second problem is that the prediction from RNNs is deterministic, which is not satisfactory in human robot interaction, since the robot needs the uncertainty level of human’s future motion for safe motion planning. The last serious problem is that the RNN models are fixed and they cannot adapt to time-varying human behaviors.

This paper aims to solve these problems by proposing a new prediction method using an adaptable neural network. Human transition model is approximated by a feedforward neural network, whose structure is simpler than the RNN, therefore, more computationally efficient. Moreover, our work on adaptable feedforward neural networks may also be extended to adaptable RNNs. To accommodate time-varying behaviors and individual differences in human motion, parameters in the last layer of the neural network are adapted online using recursive least square parameter adaptation algorithm (RLS-PAA). We also provide the uncertainty level analysis for the predictions of human motion. The uncertainty level, together with the prediction, will be sent to the motion planning module of robot. To verify the proposed algorithm, we compare it with the state-of-the-art online learning algorithm called the identifier-based algorithm [14]. Identifier-based algorithm adapts all the parameters in the offline-trained neural network model online, using gradient descent to minimize the prediction error. Results demonstrate that our method achieves a higher prediction accuracy than

* Equal contribution.

This work was supported by National Science Foundation (Award #1734109).

Y. Cheng and M. Tomizuka are with the Department of Mechanical Engineering, University of California, Berkeley, CA 94720 USA (e-mail: yujiachoeng, tomizuka@berkeley.edu).

W. Zhao is with Shanghai Jiao Tong University, Shanghai, China (e-mail: andylaw@sjtu.edu.cn).

C. Liu is with Stanford University, Stanford, CA 94305 USA (e-mail: changliuliu@stanford.edu).
the identifier-based algorithm, and the performance is stably maintained across a variety of motion categories and motion datasets. Our code is publicly available at https://github.com/msc-berkeley/Human-Motion-Prediction

The remainder of the paper is organized as follows. Section II formulates the human motion prediction problem. Section III proposes the method of adaptable neural networks. Section IV shows the performance of the proposed method and compares it with other methods. Section V discusses analyses and extensions of the proposed method. Section VI concludes the paper.

II. PROBLEM FORMULATION

Predicting human motion is important for smooth human robot interaction, in that if we know what the human is going to do, it can adapt its actions to collaborate with humans in an efficient way and plan collision-free trajectories to guarantee humans safety [15]. This paper concerns with the prediction of the movement of one human joint (e.g., wrist). When human works in close proximity to a robot, special attention should be paid to human’s hand movement. Moreover, the prediction of one joint motion should be extendable to multiple joints, which is important for whole body prediction as discussed in section V.

The transition model of human joint motion is formulated as

\[
x(k + 1) = f^*(x^*(k), a) + w_k,
\]

where \(x(k + 1) \in \mathbb{R}^{3M}\) denotes human’s \(M\)-step future trajectory state of the joint at time steps \(k+1, k+2, \ldots, k+M\) in a Cartesian coordinate system. \(M \in \mathbb{N}\) is the prediction horizon. Denoting \(p(k) \in \mathbb{R}^3\) the Cartesian position of the joint at time step \(k\), \(x(k+1)\) is a stack of \(M\) future joint positions \(p(k+1), p(k+2), \ldots, p(k+M)\). \(x^*(k) \in \mathbb{R}^{3N}\) denotes human’s past \(N\)-step trajectory of the joint at time steps \(k, k-1, \ldots, k-N+1\). It is also constructed by stacking the position vectors \(p(k), p(k-1), \ldots, p(k-N+1)\). \(a \in \mathbb{N}\) is an action label to distinguish different motions, and this label is obtained by the action recognition module of the system [15]. \(w_k \in \mathbb{R}^{3M}\) is a zero-mean white Gaussian noise. The function \(f^*(x^*(k), a) : \mathbb{R}^{3N} \times \mathbb{N}^1 \rightarrow \mathbb{R}^{3M}\) represents the transition of the human motion, which takes historical trajectory and current action label as inputs, and outputs the future positions of the joint.

Since human behavior differs greatly across individuals and is highly time-varying, function \(f^*\) may not be a time invariant function. Though \(f^*\) takes the discrete parameter action label \(a\) as one of the inputs to accommodate some of the variances, an adaptable model of \(f^*\) is still desired to account for continuous changes online in order to provide accurate prediction.

III. ADAPTABLE NEURAL NETWORKS

Since human’s motion is not only time-varying but also highly nonlinear, we propose to use an adaptable neural network to construct the model \(f^*\). By removing the output layer, the pre-trained neural network become an effective feature extractor [16], the features from which are better than handcrafted ones [17]. Therefore we only adapt the weights of output layer of the neural network online, which fixes the weights of the remaining layers, hence fixing the extracted features.

The proposed procedure is that
1) We first design a neural network architecture;
2) We train the model \(f^*\) offline;
3) During online execution, we adapt the parameters of the neural network last layer using efficient adaptation algorithm;
4) We then compute the uncertainty level of predictions given the adaptation result.

The algorithm is shown in Algorithm 1.

Algorithm 1: Adaptable neural network for human motion prediction

| Input | Offline trained neural network \(\theta\) with \(g\), \(U\) and \(W\) |
|---|---|
| Output | future trajectory \(x(k+1)\) |
| Variables | Adaptation gain \(F\), \(a\) priori mean squared estimation error of states \(X_{\hat{g}g}\), mean squared estimation error of the parameters \(X_{\hat{g}g}\), neural network last layer parameters \(\theta\), estimated rate of change \(\delta \theta\) (approximation of \(\Delta \theta\)), variance of zero-mean white Gaussian noise \(Var(w_k)\) |
| Initialization | \(F=1000\), \(A=\) column stack of \(W, X_{\hat{g}g}=0, X_{\hat{g}g}=0\), \(\lambda_1=0.998\), \(\lambda_2=1\) |

1) \(\text{while True do}\)
2) \(\text{Wait for a new joint position } p \text{ captured by Kinect and current action label } a \text{ from action recognition module;}\)
3) \(\text{Construct } s_k=[p(k), p(k-1), \ldots, p(k-N+1), a, 1]^T;\)
4) \(\text{Obtain } \Phi(k) \text{ by diagonal concatenation of } max(0, g(U, s_k));\)
5) \(\text{Update } F \text{ by (8);}\)
6) \(\text{Adapt the parameters } \theta \text{ in last layer of neural network by (6);}\)
7) \(\text{Calculate future joint trajectory } x(k+1) \text{ by (3);}\)
8) \(\text{Update } \delta \theta \text{ and calculate } X_{\hat{g}g} \text{ and } X_{\hat{g}g} \text{ by (9) and (11).}\)

A. Training the Neural Network

To train the transition model \(f^*\), we choose an \(n\)-layer neural network with ReLU activation function which takes the positive part of the input to a neuron.

\[
f^*(x^*(k), a) = W^T \max(0, g(U, s_k)) + \epsilon(s_k), \quad (2)
\]

where \(s_k = [x^*(k)^T, a, 1]^T \in \mathbb{R}^{3N+2}\) is the input vector, \(g\) denotes \((n-1)\)-layer neural network, whose weights are packed in \(U\), \(\epsilon(s_k) \in \mathbb{R}^{3M}\) is the function reconstruction.
error, which goes to zero when the neural network is fully trained. \( W \in \mathbb{R}^{n_h \times 3M} \) are the weights of the last layer, where \( n_h \in \mathbb{N} \) is the number of neurons in the hidden layer of the neural network [14].

B. Parameter Adaptation Algorithm

To accommodate both the time varying behavior of human and individual differences among different people, it is important to update the parameters online. In this paper, we applied the recursive least square parameter adaptation algorithm (RLS-PAA) with forgetting factor [18] to asymptotically adapt the parameters in the neural network.

By stacking all the column vectors of \( W \), we get a time varying vector \( \theta \in \mathbb{R}^{3Mn_h} \) to represent the weights of last layer. \( \theta_k \) denotes its value at time step \( k \). To represent the extracted features, we define a new data matrix \( \Phi_k \in \mathbb{R}^{3M \times 3Mn_h} \) as a diagonal concatenation of \( M \) pieces of \( \max(0, g(U, s_k)) \). Using \( \Phi_k \) and \( \theta_k \), (1) and (2) can be written as

\[
x(k+1) = \Phi_k \theta_k + w_k.
\]

Let \( \hat{\theta}_k \) denotes the parameter estimate at time step \( k \), and let \( \delta \theta_k = \theta_k - \hat{\theta}_k \) be the parameter estimation error. We define the a priori estimate of the state and the estimation error as:

\[
\hat{x}(k+1|k) = \Phi_k \hat{\theta}_k,
\]
\[
\hat{x}(k+1|k) = \Phi_k \hat{\theta}_k + w_k.
\]

The core idea of RLS-PAA is to iteratively update the parameter estimation \( \theta_k \) and predict \( x(k+1) \) when new measurements become available. The parameter update rule of RLS method can be summarized as:

\[
\hat{\theta}_{k+1} = \hat{\theta}_k + F_k \Phi_k^T \delta \theta_k,
\]

where \( F_k \) is the learning gain updated by:

\[
F_{k+1} = \frac{1}{\lambda_1(k)} \left[ F_k - \lambda_2(k) \frac{\Phi_k \Phi_k^T F_k}{\lambda_1(k) + \lambda_2(k) \Phi_k^T \Phi_k} \right]
\]

where \( 0 < \lambda_1(k) \leq 1 \) and \( 0 < \lambda_2(k) \leq 2 \). Typical choices for \( \lambda_1(k) \) and \( \lambda_2(k) \) are:

1) \( \lambda_1(k) = 1 \) and \( \lambda_2(k) = 1 \) for standard typical least squares gain.
2) \( 0 < \lambda_1(k) < 1 \) and \( \lambda_2(k) = 1 \) for least squares gain with forgetting factor.
3) \( \lambda_1(k) = 1 \) and \( \lambda_2(k) = 0 \) for constant adaptation gain.

C. Mean Squared Estimation Error Propagation

To guarantee safety, the uncertainty of the prediction is also quantified during online adaptation [19].

\( \delta \theta_k \) only contains information up to the \( (k-1) \)th time step, and \( \hat{\theta}_k \) is independent of \( w_k \). Thus the a priori mean squared estimation error (MSEE) \( \sum_{i=0}^{\infty} \delta \theta_i(k) = \Phi_k \hat{\theta}_k(k) \Phi_k^T + Var(w_k) \) is

\[
X_{\hat{\theta}}(k+1|k) = E \left[ \delta \theta_k(k+1|k) \right]
\]

where \( X_{\hat{\theta}}(k) = E \left[ \hat{\theta}_k(k) \hat{\theta}_k(k)^T \right] \) is the mean squared error of the parameter estimate and \( Var(w_k) \) is the variance of zero-mean white Gaussian noise.

b) Parameter estimation: Since the system is time varying, \( \delta \theta_k = \theta_{k+1} - \theta_k \neq 0 \). According to parameter estimation algorithm in (6), the parameter estimation error is

\[
\hat{\theta}_{k+1} = \hat{\theta}_k - F_k \Phi_k^T \delta \theta_k + \Delta \theta_k.
\]

The estimated parameter is biased and the expectation of the error can be expressed as

\[
E \left[ \hat{\theta}_{k+1} \right] = [I - F_k \Phi_k^T] E \left[ \hat{\theta}_k \right] + \Delta \theta_k
\]

The mean squared error of parameter estimate follows from (9) and (10):

\[
X_{\hat{\theta}}(k+1) = F_k \Phi_k^T X_{\hat{\theta}}(k) \Phi_k F_k - F_k \Phi_k^T X_{\hat{\theta}}(k) + E \left[ \hat{\theta}_{k+1} \right] \Delta \theta_k^T
\]

Since \( \Delta \theta_k \) is unknown in (10) and (11), we define \( \delta \theta_k = \hat{\theta}_k - \theta_{k-1} \), and approximate \( \Delta \theta_k \) as \( \delta \theta_k \), which is the average of \( \delta \theta_i, i = k - n_w + 1, k - n_w, ..., k \), where \( n_w \in \mathcal{N} \) is the window size.

At step \( k \), the predicted trajectory \( \hat{x}(k+1|k) \) together with the uncertainty matrix \( X_{\hat{x}}(k+1|k) \) is then sent to robot control to generate the safety constraint.

IV. RESULTS

A. Human Motion Prediction on Kinect Data

1) Data Acquisition: In order to verify the proposed human motion prediction approach, experiments are conducted when human and robot collaborate to assemble a desktop. The experimental setup is shown in Fig. A Kinect for Windows v2 is utilized to capture the trajectory of human right wrist at an approximate frequency of 20Hz. Human has two options: one is to obtain and insert the RAMs in the motherboard, and the other is to fetch and assemble the disk to the desktop case. 50 trajectories for each motion are obtained, of which 80% is utilized for offline neural network training, and the remaining is for the validation of the online adaptation algorithm. To smooth the trajectories, we use a low-pass filter \( p_s(k) = 0.6p_s(k-1) + 0.4p_s(k) \), \( p_s(k) \in \mathbb{R}^3 \) is the smoothed position of the joint at time step \( k \), which is the weighted average of joint positions \( \hat{p}(k-1) \) and \( \hat{p}(k-2) \).
measured at time step $k - 1$ and $k - 2$. We set the number of past and future joint positions $N$ and $M$ both to be 3, which implies that we are doing predictions of three time steps approximately 0.15s. The prediction horizon can be controlled by adjusting the magnitude of $M$ according to the specific applications.

2) Neural Network Training: We use a 3-layer neural network with 40 nodes in the hidden layer. The number of nodes in the input layer and the output layer is 9. The loss function is set to be L2 loss. The learning rate is set to 0.001 and the number of epochs is 100.

3) Online Adaptation: After obtaining the neural network model for motion transition, we use RLS-PAA to adapt the weights of the last layer. Since the number of nodes in the last layer is 9, and each node has 41 parameters, of which 40 correspond to the outputs from the hidden layer, and the remaining one parameter is a bias term. In total, there are 369 parameters to be adapted online. In the case that the initial values for all the parameters are set to be 10, the three parameters we randomly choose quickly settle into finite bounds as shown in Fig. 2.

4) Trajectory Prediction: Fig. 3 shows the prediction results of the right wrist. The three subplots represent three moments in human motion of fetching and assembling disk to the desktop case. In the first two subplots, human is bringing the disk near the desktop case and in the third subplot, human is inserting the disk. Suppose that the current time step is $k$, the blue line demonstrates the predicted trajectory from the beginning to $k + 3$ time steps, of which 3 ground truth future points are used to compare with predictions. Prediction points are denoted by red circles, and the ellipsoids around them are 5% error bounds, which means that we are 95% sure that the actual motion will be in the ellipsoids. Generally, the performance is good in that the prediction points are near the ground truth, and the 5% error ellipsoids bound the ground truth in most situations. Still, prediction fails sometime when motion of human changes too rapidly as shown in the middle of Fig. 3. The joint suddenly moves rapidly, and the prediction cannot track this change, so the performance deteriorates.

B. Artificial Systems

Human motion data obtained from Kinect inherently has measurement noise. Note that several factors can contribute to the effectiveness of human motion prediction, including noise-reduced measured data and well-defined adaptation procedure. In order to gain a deeper insight into the mechanism behind the proposed algorithm, we artificially simulate the human motion, where the scale of measurement noise and the noise-free trajectories can be controlled. We construct two types of artificial systems, the time varying system and the time invariant system, to test our proposed algorithm. The performance of the proposed algorithm is also compared to identifier-based algorithm on those artificial systems.

1) Time Varying System (TV): In human dynamics model (I), the future trajectory depends on the past trajectory $x^*$, however, the trajectory itself is indeed a 3D curve parameterized by a one dimensional parameter. Here we parameterize the trajectory by time $t$. We use a polynomial function to represent the $(x, y, z)$ trajectory:

$$
x(t) = ax(t + w)^2 + bx(t + w)
$$
$$
y(t) = ay(t + w)^2 + by(t + w)
$$
$$
z(t) = az(t + w)^2 + bz(t + w)
$$

where $w$ denotes the artificial noise and $t \in [0, 5s]$. The trajectory is sampled every $\Delta t = 0.05s$. It is easy to verify that given the 3D curve, the resulting dynamic model in the form of (I) is time-varying. We have applied two sets of parameters $[a_x, b_x, a_y, b_y, a_z, b_z]$ to generate two different simulated motions, $[0.4, −2, 0, 0.9, 0, 1.05]$ and $[0.41, −1.9, 1, 0.9, 0, 0.95]$, the unit for three axes is $m$. We also add artificial noise to the artificial motion trajectory data since measurement noise exists in real world data. Therefore, uniformly distributed noise $w_n$ in the range $[-1, 1]$ is added to $t$. For each motion kind we simulate 50 independent trials.

2) Time Invariant System (TI): In contrast to the time varying system, the time invariant system has constant model $f$ that does not depend on time. Here we also choose a quadratic formula to parameterize the time-invariant state.
transition model:
\[
\begin{align*}
  x(t + \Delta t) &= a_x x(t)^2 + b_x x(t) + w \\
  y(t + \Delta t) &= a_y y(t)^2 + b_y y(t) + w \\
  z(t + \Delta t) &= a_z z(t)^2 + b_z z(t) + w.
\end{align*}
\]

We obtain the TI trajectory with the following strategy: we first randomize the initial position, and then at each sample iteration we get a new position using the quadratic state transition model above provided with the position from last iteration. In the experiment setting, we use two sets of parameters \([a_x, b_x, a_y, b_y, a_z, b_z]\) to represent two kinds of motion classes as well, \([0.06, 0.92, 0, 0, 0, 1.05]\) and \([0.061, 0.93, 0, 1.05, 0, 0.96]\), the unit for three axes is dm. Uniformly distributed noise is also added to the simulated data.

C. Comparison

To demonstrate the effectiveness of the proposed method, we evaluate the proposed algorithm on four different human motion datasets. They are artificial time invariant motion data, artificial time varying motion data, human motion data collected by Kinect and CMU motion dataset\(^1\). From CMU dataset, we choose to use Mocap data of walking, runing and jumping of all subjects. To verify our algorithm, we compare it with the state-of-the-art online learning algorithm called Identifier-based algorithm. Identifier-based algorithm adapts all the parameters in the offline-trained neural network model online using gradient descent to minimize the prediction error. Same architecture of the neural network as specified in [14] is utilized for fair comparison. Both neural networks are trained offline for 100 epochs before online adaptation.

We evaluate the performance of online adaption algorithms by prediction errors. The comparison between identifier-based algorithm and our methods is demonstrated in Fig. 4. We also compare the prediction errors by the neural network models without online adaptation. RLS method results in smallest prediction errors on all the datasets, which demonstrates the effectiveness of our proposed algorithm. Mean squared estimation error (MSEE) of all methods are shown in Table I. Compared to identifier-based algorithm, RLS has much smaller MSEE across four different datasets in all \(x, y, z\) axes.

As for the training efficiency, since gradient operation is expensive to compute for large neural networks, we observed that it takes roughly 0.375s for identifier-based algorithm to adapt one motion sample using standard gradient operation whereas it only takes 0.031s for our proposed method to adapt one sample. Our method is better for real-time applications. For identifier-based algorithm that adapts all parameters in the neural network, even though it is possible to accelerate gradient operation using central difference approximation, the computation complexity grows exponentially as the complexity of the neural network grows.

All the experiments are performed on the MATLAB 2016 platform with 2.7GHz Intel Core i5 Processor.

V. DISCUSSION

The objective of this paper is to uncover a robust and general human motion transition model that can adapt to

\(^{1}\)Available at \[http://mocap.cs.cmu.edu/motcat.php\]
Fig. 4: Prediction error comparison between RLS-PAA (blue system) and Identifier-based (red system) algorithm on four datasets. From top to bottom, each row is the experiment result tested on artificial time invariant system data, artificial time variant system data, Kinect data, and CMU dataset. In the experiment, when a new measurement is available, three future positions are predicted, and they are shown in the separate three columns respectively. The vertical black dash lines denote the boundaries of different motion classes.
different motion patterns, and capture the uncertainty level of the prediction in real time. Our approach combines offline training and online adaptation for function approximation, which takes the advantages of both methods. Offline training of the neural network extracts global features from the data. Online adaptation changes the way that the global features are combined by adjusting the coefficients in the last layer of the network locally to minimize real time prediction error. Onerous model coefficient-tuning is not required in our approach.

A. Analyses
State-of-the-art identifier-based adaptation algorithm requires heavy coefficient tuning. The performance of identifier-based algorithm highly relies on the scale of update step size. The computation of the gradient has inertia that it cannot adapt the sudden change quickly. However, sudden change of velocity happens a lot in human motion. Therefore, some peak prediction error can be observed from time to time as shown in Fig. 4, especially at the beginning of each motion trial, since there is a clear velocity jump between the beginning and the end of two different trials.

The number of past joint positions being considered has impact on the prediction performance. Online RLS algorithm looks back into historical trajectory with exponentially decayed weights. The forgetting factor controls how far back the algorithm is using the past information. In our experiment on Kinect data, the optimal forgetting factor is 0.9998. Note that to accommodate a more rapidly changing motion, the forgetting factor may be set smaller so that the algorithm looks back in a short range.

In many human robot interaction applications, human often work with robots over tables, standing or sitting in a fixed position where only the human upper body prediction is required. Note that human upper body can be viewed as a fixed-base cascade robot arm, which can be represented by a kinematic chain model. In our experiments, we focus on motion prediction for one wrist joint, which can be viewed as the end point position in the chain model. Whole arm movement can be predicted either using inverse kinematics or dynamic simulation given the prediction of the wrist position.

B. Extensions
Our proposed algorithm can be easily applied to many fields and extended by combination with other algorithms. Generally speaking, we can apply the method to many other time series data prediction, such as vehicle and pedestrian motion prediction. In these cases, we regard the vehicles and pedestrians as joints in our method, and adapt the model and obtain uncertainty level online, which is beneficial in autonomous driving. Our proposed algorithm can also be combined with other algorithms by modeling the velocity state transition pattern, which can be used to adjust the update step size.

VI. CONCLUSION
This paper proposed a novel method using an adaptable neural network to predict human motion, which is capable of adapting the model online and provides uncertainty level for safety constraints. Offline trained neural network takes the historical joint trajectory as input and outputs the predictions. In online test, the parameters of the last layer in the neural network model is adapted to accommodate individual differences and time-varying behaviors. The extensive experiment results demonstrate that our method outperforms the state-of-the-art method with a significant margin on the majority of the motion datasets in terms of prediction error. Moreover, our model is much more computationally efficient and is free of onerous tuning. The performance is robust across different motion categories and datasets.

REFERENCES
[1] K. Yamazaki, R. Ueda, S. Nozawa, M. Kojima, K. Okada, K. Matsumoto, M. Ishikawa, I. Shimoyama, and M. Inaba, “Home-assistant robot for an aging society,” Proceedings of the IEEE, vol. 100, no. 8, pp. 2429–2441, 2012.
[2] W. Knight, “Smart robots can now work right next to auto workers,” MIT Technology Review, vol. 17, 2013.
[3] M. A. Diftler, J. Mehling, M. E. Abdallah, N. A. Radford, L. B. Bridgewater, A. S. Sanders, R. S. Askew, D. M. Linn, J. D. Yanokoski, F. Permenter, et al., “Robonaut 2-the first humanoid robot in space,” in Robotics and Automation (ICRA), 2011 IEEE International Conference on. IEEE, 2011, pp. 2178–2183.
[4] A. Gupta, J. Martinez, J. J. Little, and R. J. Woodham, “3d pose from motion for cross-view action recognition via nonlinear circulant temporal encoding,” in Proceedings of the IEEE conference on computer vision and pattern recognition, 2014, pp. 2601–2608.
[5] L. Kovar, M. Gleicher, and F. Pighin, “Motion graphs,” in ACM SIGGRAPH 2008 classes. ACM, 2008, p. 51.
[6] N. F. Troje, “Decomposing biological motion: A framework for analysis and synthesis of human gait patterns,” Journal of vision, vol. 2, no. 5, pp. 2–2, 2002.
[7] Z. Peng, T. Genewein, and D. A. Braun, “Assessing randomness and complexity in human motion trajectories through analysis of symbolic sequences,” Frontiers in human neuroscience, vol. 8, p. 168, 2014.
[8] M. Kohler et al., Using the Kalman filter to track human interactive motion: modelling and initialization of the Kalman filter for translational motion. Dekanat Informatik, Univ., 1997.
[9] A. Bruce and G. Gordon, “Better motion prediction for people-tracking,” in Proc. of the Int. Conf. on Robotics & Automation (ICRA), Barcelona, Spain, 2004.
[10] M. Kalakrishnan, S. Chitta, E. Theodorou, P. Pastor, and S. Schaal, “Stomp: Stochastic trajectory optimization for motion planning,” in Robotics and Automation (ICRA), 2011 IEEE International Conference on. IEEE, 2011, pp. 4569–4574.
[11] D. Wu and L. Shao, “Leveraging hierarchical parametric networks for skeletal joints based action segmentation and recognition,” in Proceedings of the IEEE conference on computer vision and pattern recognition, 2014, pp. 724–731.
[12] P. Ghosh, J. Song, E. Aksan, and O. Hilliges, “Learning human motion models for long-term predictions,” in 3D Vision (3DV), 2017 International Conference on. IEEE, 2017, pp. 458–466.
[13] A. Alahi, K. Goel, V. Ramanathan, A. Robicquet, L. Fei-Fei, and S. Savarese, “Social Istm: Human trajectory prediction in crowded spaces,” in Proceedings of the IEEE Conference on Computer Vision and Pattern Recognition, 2016, pp. 961–971.
[14] H. C. Ravichandar and A. P. Dani, “Human intention inference using expectation-maximization algorithm with online model learning,” IEEE Trans. Automation Science and Engineering, vol. 14, no. 2, pp. 855–868, 2017.
[15] C. Liu, T. Tang, L. Hsien-Chung, Y. Cheng, and M. Tomizuka, “Serocs: Safe and efficient robot collaborative systems for next generation intelligent industrial co-robots,” arXiv preprint arXiv:1809.08215, 2018.
[16] B. Athiwaratkun and K. Kang, “Feature representation in convolutional neural networks,” arXiv preprint arXiv:1507.02313, 2015.
[17] A. Sharif Razavian, H. Azizpour, J. Sullivan, and S. Carlsson, “Cnn features off-the-shelf: an astounding baseline for recognition,” in Proceedings of the IEEE conference on computer vision and pattern recognition workshops, 2014, pp. 806–813.

[18] G. C. Goodwin and K. S. Sin, Adaptive filtering prediction and control. Courier Corporation, 2014.

[19] C. Liu and M. Tomizuka, “Safe exploration: Addressing various uncertainty levels in human robot interactions.” in ACC, 2015, pp. 465–470.