Fuzzy Evaluation Algorithm for System Effectiveness of Wireless Sensor Networks

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Abstract—Evaluation of System Effectiveness (SE) plays a significant role in network design, construction, optimization, etc. of Wireless Sensor Networks (WSNs). This paper develops a rational and comprehensive five-layer indicator model which incarnates SE or monomial efficiency of WSNs. Also, we propose a valid evaluation model HFCE with Analytic Hierarchy Process (AHP) and Fuzzy Comprehensive Evaluation (FCE), both of which combined together is suitable for hierarchical indicator model and multiattribute decision analysis of WSNs. The results obtained from simulation demonstrate practicability of indicator model and accuracy of evaluation model.

Keywords—evaluation model, indicator model, system effectiveness, wireless sensor networks

I. INTRODUCTION

Wireless Sensor Networks (WSNs) with heterogeneous sensing, wireless communication, and data processing are widely applied in various fields [1]-[3]. So it poses great challenges to System Effectiveness (SE) which leads direct impetus to its application. Methodical and efficient solution to SE is effectiveness evaluation through which it can play a leading role in system design by comprehensive analysis of key influencing factors and guide system optimization with identifying some problems during design, development, and operating stages.

The current research of SE for WSNs is mainly focused on monomial effectiveness evaluation, such as QoS, localization, network protocol performance, and energy consumption, etc. For QoS evaluation, there are some available models and mediums. Based on established QoS model and fuzzy logic, a relative holistic conclusion is achieved by studying the two-way mapping between network layer and application layer [4]-[5]. Still, in terms of various evaluation contents and targets, Rough Set theory is capable of condensing evaluation frame of WSNs which is composed of five parts [6]. As far as localization in WSNs, some experiments are carried out indoors or in rainforests to verify the assessment with localization techniques in [7] and [8]. With respect to the evaluation of MAC, some parameters matching the tested features are brought in to collect the packets and collision information [9]. Moreover, a classical mathematical model—Markov is employed in node behavior of MAC protocols on estimation performance, and filtering model—Kalman is used to illustrate the approaches of multi-sensor [1]. With regard to the vital aspect system energy consumption, novel fuzzy metric logic is introduced to further acquire the superiority of different clustering schemes so as to prolong lifetime [10]-[12].

All hereinabove center on simplex approach to evaluate some part of WSNs performance, however, owing to some unique characteristics of WSNs, such as limited energy, non-end-to-end network, redundant nodes and data, etc. traditional standard and method of effectiveness evaluation cannot meet requirements of WSNs. So it is essential to investigate indicator model and evaluation model. The former one is the basis of SE, and the latter one concerns core technology. It is hoped that this problem will be partly resolved with our proposed approach.

The remainder of this paper is organized as follows. Section II introduces indicator model with 5 levels and evaluation model with joint method HFCE. Section III presents evaluation method under classification of indicators. In Section IV, the simulation testing on evaluation and sensitivity of WSNs is conducted. Finally, our conclusions are presented in Section V.

II. BUILDING RELATED MODELS

A. Indicator Model for WSNs

Indicator model abides by objectivity, decomposition, testability, integrity, and independence. Referring to the knowledge mentioned above, we put forward a topdown five-layer indicator model which contains target layer, criterion layer, subcriterion layer, evaluation indicator layer, and scale parameter layer. Target layer the ultimate goal indicates System Effectiveness; criterion layer is composed of QoS, energy consumption, network management, and other crucial factor in view of system application; subcriterion layer represents significant task of each monomial efficiency; evaluation indicator layer designates primary aspects of each task; scale parameter layer reflects inherent characteristic of WSNs. This indicator model affords relatively rounded indicators, so the concrete indicator should be confirmed by its application. The main body frame of indicator model is expressed in Table I, II, III, IV, and V.

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### Table I. Indicator Model for WSNS

| Target layer | Criterion layer |
|--------------|-----------------|
| $E\text{(System Effectiveness)}$ | $u_1$, QoS |
|         | $u_2$, Energy management |
|         | $u_3$, Network management |
|         | $u_4$, Other factors |

### Table II. Criterion Layer-QoS Indicator Model

| Criterion layer | Subcriterion layer | Evaluation indicator layer |
|-----------------|--------------------|-----------------------------|
| $u_{11}$ Application layer | $u_{111}$ Response time |
| | $u_{112}$ Time synchronization |
| | $u_{113}$ Node location |
| | $u_{114}$ Data accuracy |
| | $u_{115}$ Processing latency |
| | $u_{116}$ System lifetime |
| $u_{12}$ Transmission layer | $u_{121}$ End-to-End latency |
| | $u_{122}$ End-to-End bandwidth |
| $u_{13}$ Network layer | $u_{131}$ Expansibility |
| | $u_{132}$ Path latency |
| | $u_{133}$ Congestion probability |
| | $u_{134}$ Energy efficacy |
| | $u_{135}$ Routing maintenance |
| | $u_{136}$ Routing robustness |
| $u_{14}$ MAC layer | $u_{141}$ Throughput |
| | $u_{142}$ Accessing time |
| | $u_{143}$ Energy efficacy |
| | $u_{144}$ Transmission reliability |
| $u_{15}$ Physical layer | $u_{151}$ Channel speed |
| | $u_{152}$ RF power |
| | $u_{153}$ Processing capability |
| | $u_{154}$ Sensing accuracy |
| | $u_{155}$ Sensing range |
| | $u_{156}$ Sensing power |

### Table III. Criterion Layer-Energy Consumption Indicator Model

| Criterion layer | Subcriterion layer |
|-----------------|--------------------|
| $u_3$, Energy consumption | $u_{31}$ Application layer |
| | $u_{32}$ Transmission layer |
| | $u_{33}$ Network layer |
| | $u_{34}$ MAC layer |
| | $u_{35}$ Physical layer |

### Table IV. Criterion Layer-Network Management Indicator Model

| Criterion layer | Subcriterion layer | Evaluation indicator layer | Scale parameter layer |
|-----------------|--------------------|-----------------------------|-----------------------|
| $u_{31}$ Information acquisition capability | $u_{311}$ Accuracy of information acquisition |
| | $u_{312}$ System reliability |
| | $u_{313}$ Congestion probability |
| | $u_{314}$ Energy efficacy |
| | $u_{315}$ Processing latency |
| | $u_{316}$ System lifetime |
| | $u_{32}$ Information processing capability |
| | $u_{321}$ End-to-End latency |
| | $u_{322}$ End-to-End bandwidth |
| | $u_{323}$ End-to-End reliability |
| $u_3$, Network management | $u_{33}$ System viability |
| | $u_{331}$ System serviceability |
| | $u_{332}$ System invulnerability |
| | $u_{333}$ System control capability |
| | $u_{334}$ Anti-jamming ability |
| | $u_{335}$ Centralized control ability |
| | $u_{336}$ Topological control |
| | $u_{34}$ Security |
| | $u_{341}$ Data leakage rate |
| | $u_{342}$ Data presentation error |
| | $u_{343}$ Data storage capacity |
| | $u_{344}$ Anti-electromagnetic ability |
| | $u_{345}$ Anti-human disturbance |
| | $u_{346}$ Radio frequency interference |

### Table V. Criterion Layer-Other Factors Indicator Model

| Criterion layer | Subcriterion layer |
|-----------------|--------------------|
| $u_4$, Other factors | $u_{41}$ Environment factor |
| | $u_{42}$ People factor |
| | $u_{43}$ Risk factor |
| | $u_{44}$ Cost factor |

### B. Evaluation Model

To formally specify SE evaluation requirements in WSNs, a proper evaluation model is needed. In terms of system, evaluation model involves systemic design and adaptive strategy both of which rest with indicator model. So pretreatment origins in the classification of indicator. Furthermore, HFCE algorithm is a satisfactory solution to complete multiple criteria decision making (MCDM) and to eliminate fuzziness of indicators. The result can be in favor of system design or optimization. Figure 1 illustrates the integrated evaluation model.
III. EVALUATION METHOD

A. Pretreatment of Indicators

Whether can be measured is the standard principle of indicator classification, hence we divide all indicators into two types: quantitative indicators and qualitative indicators. In order to eliminate incommensurability and contradictoriness, pretreatment through some mathematics method is significant for universalizing the criteria of measurement with different type of indicator.

1) Pretreatment of Quantitative Indicators

By the relationship between indicator value and SE, quantitative indicators can be partitioned into: positive influence indicator, negative influence indicator, and positive and negative influence indicator. If the line turns out to be positive slope, this indicator can be defined as positive influence indicator, negative influence indicator, and positive and negative influence indicator. If the line turns out to be negative slope, this indicator can be defined as positive and negative influence indicator. On the contrary, it is known as negative influence indicator. Besides, positive and negative influence indicator is portrayed with a peak turning point in the growth of influence indicator. Besides, positive and negative influence indicator are measurable indicator value, where measurable indicator value, \( x_{\text{opt}} \) and \( x_{\max} \) respectively represent upper and lower bound of \( x \). Meanwhile, \( x_{\text{opt}} \) is the optimal value in positive and negative influence indicator, and the calculation \( v \) is the input variable of fuzzy evaluation method.

2) Pretreatment of Qualitative Indicators

Under the complexity of objective environment and fuzziness of subjective judgment, qualitative indicators are often decided by some experienced experts. At this period, we should confirm related specialist by all of qualitative indicators and apportion some evaluation indicators to them.

B. Evaluation Method

On the basis of hierarchic indicator model and fuzzy correlation of indicators, a joint evaluation method Analytic Hierarchy Process (AHP) and Fuzzy Comprehensive Evaluation (FCE) is introduced. By simulating iterative operation with weight obtain from AHP and degree of membership offered by FCE, final evaluation value and further quantitative analysis can be got.

1) Solution to Weight

In accordance with hierarchic indicator model, the most appropriate solution to weight is AHP consisting of the following steps.

S1) Through paired comparison between two indicators with the same level, judgment matrix can be constructed as

\[
A = (a_{ij})_{n \times n}.
\]  

S2) Calculate maximum eigenvalue \( \lambda_{\text{max}} \) and maximum eigenvector vector \( W \) of the judgment matrix.

S3) Check consistency ratio CR as

\[
CI = (\lambda_{\text{max}} - n)/(n-1)
\]  

\[
CR = CI/RI
\]  

where \( n \) is the order of the matrix; \( RI \) and \( CI \) are severally on behalf of random consistency index, consistency check index.

If \( CR<0.1 \), the consistency of judgment matrix fulfills the request and \( W \) is the weight vector we want. Otherwise, the judgment matrix should be reconstructed. Accordingly, boundary value of maximum eigenvalue \( \lambda_{\text{max}} \) can be got as

\[
\lambda_{\text{max}} = (CR \times RI)^*(n-1) + n.
\]

The boundary of maximum eigenvalue is showed in Table VI.

| TABLE VI. BOUNDARY VALUE OF MAXIMUM EIGENVALUE |
|-----------------|-----------------|-----------------|-----------------|-----------------|
| \( \lambda_{\text{max}} \) | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 |
| 1.16 | 3.116 | 4.288 | 5.448 | 6.62 | 7.792 | 8.987 | 10.16 |

2) Solution to Single-stage Degree of Membership

Degree of membership denotes quantitative possibility of a factor assessed as some qualitative degree. The valid means for single-stage degree of membership depends on categories of indicators; trapezoidal fuzzy distribution is selected for quantitative indicators and typical Delphi is applied for qualitative indicators.

a) Disposal of quantitative indicators

Assignment method-trapezoidal fuzzy distribution is a universal and effective solution to different level fuzzy phenomenon. Trapezoidal fuzzy function is given by

\[
r(x) = \begin{cases} 
0, & x \leq a \\
\frac{x-a}{b-a}, & a < x < b \\
1, & b \leq x \leq c \\
\frac{d-x}{d-c}, & c < x < d 
\end{cases}
\]  

\[ (8) \]
where four parameters \(a, b, c,\) and \(d\) refers to each value of vertexes in trapezoidal abscissa.

b) Disposal of qualitative indicators

Delphi can acquire quantitative results by experienced experts’ judgments. Such is suitable for qualitative indicator which can only be measured by subjective opinions. Suppose \(V\) be evaluation set and \(r_{ij}\) indicating factor \(i\) assessed as \(V_j\) be degree of membership, there are \(s\) from \(m\) experts designating degree of membership of factor \(i\) as \(r_{ji}\). Then degree of membership of each qualitative indicator can be got as

\[
R = \begin{bmatrix}
    R | u_1 \\
    R | u_2 \\
    \vdots \\
    R | u_s \\
\end{bmatrix}
\]

The results in a) or b) by rules formulate fuzzy relation matrix \(R\) and can be showed as

\[
r_{ij} = s/m. \quad (9)
\]

3) Solution to Multi-stage Degree of Membership

As the amount of level in indicator model is different, multi-stage method is required. From the lowest level, weight and degree of membership of each indicator can be deduced respectively through AHP and FCE presented in 1) and 2), through which degree of membership in upper level can be got by \(M(\ast, \ast)\) operator.

4) Joint Method

It ranges over HFCE joint method which contains both single-stage algorithm and multi-stage theory which is admissible depends upon the level of indicator. So from the bottom up iterative and crossover operation brings the degree of membership in upper level can be got under certain conditions.

IV. SIMULATION ANALYSIS

A. Evaluation Set and Factor Set

Evaluation set is composed of different assessment grades which are the natural language for subjective judgments of some indicator. So it can be set as \(V = \{\text{excellent, good, normal, bad}\}\), and the corresponding evaluation fuzzy set is concretized as Table III.

| evaluation level \(v\) | \(a\) | \(b\) | \(c\) | \(d\) |
|------------------------|-----|-----|-----|-----|
| excellent              | 0.9 | 1   | 1   | 1   |
| good                   | 0.7 | 0.8 | 0.9 | 1   |
| normal                 | 0.5 | 0.6 | 0.7 | 0.8 |
| bad                    | 0   | 0   | 0.5 | 0.6 |

Factor set are equal to indicator model; target layer, criterion layer, subcriterion layer, evaluation indicator layer, and scale parameter layer correspond to the first, second, third, fourth, and fifth level, respectively.

B. Measurement of Weight

Take false alarm rate \((u_{3121})\), target discovery probability \((u_{3122})\), and target identification probability \((u_{3123})\) in scale parameter layer as example, all of which are factors of object identification quality. After thorough consideration, a judgment matrix is built as Table IV which meets the consistency requirements.

| \(u_{3121}\) | \(u_{3122}\) | \(u_{3123}\) |
|--------------|--------------|--------------|
| \(u_{1121}\) | 1             | 1/5          | 1/3          |
| \(u_{1122}\) | 5             | 1            | 3            |
| \(u_{1123}\) | 3             | 1/3          | 1            |

Then the weight vector \(W_{41}^4\) (superscript and subscript stand for the grade of target factor and concrete target factor) can be described as

\[
W_{41}^4 = \begin{bmatrix} w_{411}, w_{412}, w_{413} \end{bmatrix} = (0.103298, 0.650738, 0.245964)
\]

According to the method revealed above, weight vectors in five-grade factor sets can be calculated with the same way, and can be expressed as

\[
W_{41}^4, W_{42}^4, W_{43}^4, W_{44}^4, W_{45}^4, W_{46}^4, W_{47}^4, W_{48}^4, W_{49}^4, W_{410}^4, W_{411}^4, W_{412}^4, W_{413}^4, W_{414}^4, W_{415}^4, W_{416}^4, W_{417}^4, W_{418}^4, W_{419}^4, W_{420}^4
\]

C. Measurement of Degree of Membership

1) Degree of Membership in the Fifth Level of Factor Set

On account of connection between type of indicators and approaches to degree of membership, the coping mechanism with quantitative indicator-false alarm rate \((u_{1121})\) abides by homologous solution. In accordance with practice, it is regarded as negative influence indicator which emerges crosscurrent phenomenon with system effectiveness, so its value is set 0.2 as minimum, 0.52 as current value, and 0.8 as maximum. Then the degree of membership of this indicator turns out to be a vector \(r_{u_{1121}} = (0, 0, 0, 1)\). After another two degree of membership of indicator \(u_{1122}\) and \(u_{1123}\) are gained, these vectors are organized as a matrix \(R_{u_{112}}^4\) in order, where

\[
R_{u_{112}}^4 = \begin{bmatrix} r_{u_{1121}}, r_{u_{1122}}, r_{u_{1123}} \end{bmatrix} = \begin{bmatrix} 0 & 0 & 0 & 1 & 0.833000 & 0.167000 \\ 0 & 0.200000 & 0.800000 & 0 \end{bmatrix}
\]

Rest of degree of membership in this level can be acquired by the same way and expressed as
2) Degree of Membership in the Second, Third, and Fourth level of Factor Set

There are two kinds of factors in the second, third, and fourth level of factor set: one containing lower level indicators, and the other not. The former one exploits consequences of its lower level which become input variables through $M(\cdot, \cdot)$ calculation; the latter one employs the same way as 1). Hence the ciphered consequences are combined into matrixes under the same level which prepares for the upper interactive computation. The detailed process is showed as

$$R^2_{m_1} = \begin{bmatrix} r_{m_1} = W^{i_1} \cdot R^{i_1}_{m_1} \\ r_{m_2} = W^{i_2} \cdot R^{i_2}_{m_2} \\ \vdots \\ r_{m_n} = W^{i_n} \cdot R^{i_n}_{m_n} \end{bmatrix}, \quad r^2 = \begin{bmatrix} r_{m_1} \\ r_{m_2} \\ \vdots \\ r_{m_n} \end{bmatrix}$$

$$R^2_{m} = \begin{bmatrix} r_{m_1} = W^{i_1} \cdot R^{i_1}_{m_1} \\ r_{m_2} = W^{i_2} \cdot R^{i_2}_{m_2} \\ \vdots \\ r_{m_n} = W^{i_n} \cdot R^{i_n}_{m_n} \end{bmatrix}, \quad R^2 = \begin{bmatrix} r_{m_1} \\ r_{m_2} \\ \vdots \\ r_{m_n} \end{bmatrix}$$

$$R^2 = \begin{bmatrix} r_{m_1} = W^{i_1} \cdot R^{i_1}_{m_1} \\ r_{m_2} = W^{i_2} \cdot R^{i_2}_{m_2} \\ \vdots \\ r_{m_n} = W^{i_n} \cdot R^{i_n}_{m_n} \end{bmatrix}, \quad R^2 = \begin{bmatrix} r_{m_1} \\ r_{m_2} \\ \vdots \\ r_{m_n} \end{bmatrix}$$

3) Evaluation result

Based upon the evaluation fuzzy set defined at the beginning, we can acquire its mapped value which is revealed as $V = \{0.9, 0.8, 0.7, 0.6\}$. The evaluation results in the first and second level which embody the whole system effectiveness or different single-stage efficacy under specific design scheme are respectively named as $F, F_{m_1}, F_{m_2}, F_{m_3}$, where

$$F = V \cdot W^2_{m_1} \cdot R^2_{m_1} \cdot 100$$

$$F_{m_1} = V \cdot R^2_{m_1} \cdot 100$$

$$F_{m_2} = V \cdot R^2_{m_2} \cdot 100$$

$$F_{m_3} = V \cdot R^2_{m_3} \cdot 100$$

The qualitative result can be got as Table IX.

| result (F) | 100 ≤ F ≤ 85 | 85 < F ≤ 75 | 75 < F ≤ 65 | F < 65 |
|------------|--------------|-------------|-------------|--------|
| result     | excellent    | good        | normal      | bad    |

D. Indicator Sensitivity Analysis

It is assumed that indicator is independent so as to get rid of the interaction among indicators. Indicator sensitivity involves the influence degree of SE caused by some indicator, and under given conditions can be derived as

$$\phi_E = \frac{\Delta E}{\Delta B}$$

where $\Delta E$ is the change value of SE and $\Delta B$ is equivalent change value of degree of membership.

Take system effectiveness under certain circumstance as example, the relationship between system effectiveness and degree of membership can be showed as Figure 2, 3, 4, and 5.

![Figure 2](image-url)  
Relationship between SE and degree of membership in QoS

![Figure 3](image-url)  
Relationship between SE and degree of membership in energy
Figure 4. Relationship between SE and degree of membership in network management

Figure 5. Relationship between SE and degree of membership in other factor

Indicator sensitivity can be got as (11) and illustrated as Figure 6. From the figure, slopes of application layer in QoS and MAC layer in Energy are bigger than any other layer, so they are more sensitive than others in this case. In practice, we should promote its performance as much as possible under the same conditions.

V. CONCLUSION

From the perspective of application, this paper mainly studies indicator model and evaluation method for WSNs. So we propose a universal hierarchy model which contains not only subjective factors but also objective factors, and HFCE theory with some improvement, such as indicator classification, pretreatment, etc. Simulation manifests these models combined together can directly reflect SE and some individual efficacy, and furthermore, from its result and sensitivity analysis it can render assistance to system design, development, and optimization.

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