Spatial confinement – rapid 2D $F^-$ diffusion in micro- and nanocrystalline $\text{RbSn}_2\text{F}_5$†

Maria Gombotz,*a Sarah Lunghammer,a Stefan Breuer,a,b Ilie Hanzu,a,b Florian Preishuber-Pflügl,a and H. Martin R. Wilkeningab

Diffusion of small ions in materials with confined space for translational dynamics can be quite different to isotropic (3D) diffusion, which is found in the majority of solids. Finding credible indications for 2D diffusion is not as easy as it looks at first glance, especially if only powder samples are available. Here we chose the ternary fluoride $\text{RbSn}_2\text{F}_5$ as a new model system to seek out low-dimensional anion diffusion in a nanocrystalline material. We prepared $\text{RbSn}_2\text{F}_5$ via mechanochemically-assisted solid state synthesis and used both ac conductivity spectroscopy and spin-lock NMR relaxation measurements to find evidence that the fluorine ions preferably diffuse between the Rb-rich layers. In both cases the diffusion induced spin-lock NMR rates are only consistent with conductivity data if they are analyzed with the semi-empirical spectral density function for 2D jump diffusion as introduced by P. M. Richards [Solid State Commun., 1978, 25, 1019].

1 Introduction

Solid-state ionic conductors represent an essential component in microelectronics and devices to electrochemically store electricity.1−4 In the last ten years, quite a number of new compounds with exceptionally fast ion transport have been presented.5−12 In particular, highly conducting Li-bearing and Na-containing materials were developed to serve as non-flammable electrolytes in battery applications.12−15 Also cation-mixed fluorides,16,17 such as $\text{La}_{1−x}\text{Ba}_{x}\text{F}_3$ (see ref. 18−21, and $\text{Ba}_{1−x}\text{Ca}_x\text{F}_2$ (0 < $x$ < 1), see ref. 22, re-entered the scientific stage as they might be used as solid electrolytes in fluorine-based energy storage systems.21,24 Such ternary fluorides are anticipated to take a leap forward in micro- and nanocrystalline $\text{RbSn}_2\text{F}_5$ that 2D diffusion prevails.26−29 The same troubles hold for 1D diffusion taking place along or inside the channels.30,31 Intrachannel and intralayer hopping processes may water the reasoning for 1D or 2D diffusion down.

Only few examples have been presented in literature26,27 for which rapid 2D diffusion of Li, Na or F ions has either unequivocally been shown or at least strongly anticipated. These examples include Na-beta18-alumina,33−35 cathode materials based on $\text{Li}_2\text{CoO}_2$ (y ≤ 1) and $\text{LiFePO}_4$,36,37 Li containing transition metal sulfides (or selenides), such as $\text{Li}_2\text{TiS}_2$ (0 < $x$ ≤ 1)38−41 or $\text{Li}_2\text{NbS}_2$ (0 < $x$ ≤ 1),42 hexagonal $\text{LiBH}_4$,43 polycrystalline $\text{ZrBe}_2\text{H}_4$,44,45 and the ternary fluorides $\text{PhSnF}_4$, see ref. 43 and 44, and $\text{BaSnF}_4$.46 In some of these examples only a multi-method approach turned out to be successful to show that low-dimensional diffusion is present. For $\text{Li}_2\text{MS}_2$ (M = Ti, Nb) and $\text{ZrBe}_2\text{H}_4$, the use of variable-frequency nuclear magnetic resonance (NMR) relaxation measurements turned out to be successful to prove low-dimensional diffusion as the main motional process. For instance, McDowell et al.26 impressively showed via variable-frequency 1H NMR spin–lattice relaxation measurements that the protons in the metal-hydride $\text{ZrBe}_2\text{H}_4$ are indeed subjected to 2D diffusion.

For many cathode materials, which are used in insertion batteries,37,46−48 the NMR technique will, however, be of very limited use as paramagnetic centers cause short relaxation times which drastically narrow the time window needed for dimensionality analyses. In addition, strong spin-electron interactions govern...
the NMR relaxation rates rather than diffusive motions. Focussing here on rapid anion dynamics, ternary fluorides provide some very encouraging materials useful as model substance to test NMR relaxation models proposed for 2D diffusion.49–51 Here, RbSn2F5 attracted our attention. It belongs to the family of the pseudo-binary system MF-SnF2 where M is a monovalent cation such as Rb+, K+, Na+ or Cs+.52 Within this family RbSn2F5 offers the highest ion conductivity53 followed by KSn2F5 and NaSn2F5.54,55 Up to now it has only been prepared by solid-state reaction52 or hydrothermal synthesis in aqueous solution as first reported by Donaldson and O’Donoghue in 1964.56 In 1987 the structure of KSn2F5, to which RbSn2F5 is isostructural, was resolved as being trigonal, i.e., crystallizing with the space group P3.57 Later structure refinement was also carried out by Yamada et al.32 In Fig. 1 the crystal structure of RbSn2F5 is illustrated, which clearly shows the two-dimensional nature of this compound. In 1991 Hirokawa et al.38 suggested to interpret NMR data by using a 2D spectral density. Later, in 2004, Yamada et al.32 pointed out that also conductivity isotherms are in line with low-dimensional transport. A direct comparison of results from both NMR and conductivity spectroscopy is, however, still missing. While earlier studies focussed on coarse-grained polycrystalline samples with μm-sized crystallites, F self-diffusion in nanocrystalline RbSn2F5 has not been reported yet. Thus, the present study also aims at discussing possible effects on 2D diffusion in RbSn2F5 when the mean crystallite size is reduced to ca. 20 nm.

For this purpose, that is, to compare F diffusion in microcrystalline RbSn2F5 with that in the nanocrystalline form, we synthesized the layer-structured fluoride employing a mechanochemically-assisted ceramic route. Using a one pot synthesis, nanocrystalline RbSn2F5 was directly obtained after high-energy ball milling59 the binary starting materials RbF and SnF2. Through soft annealing we converted the as-prepared material into a microcrystalline sample. Spin-lock 19F NMR60 instead of ordinary spin-lattice relaxation NMR61 was used to record purely diffusion-controlled relaxation rates. For non-nanocrystalline RbSn2F5 the NMR rates are consistent with results from conductivity measurements only if we analyse the NMR rate peak with the model of Richards49,62 introduced for 2D jump diffusion. This result is also consistent with the electrical responses seen by conductivity spectroscopy. These findings, being in close agreement to results from literature,32 build the basis for the analysis of F anion dynamics in nanocrystalline RbSn2F5.

2 Experiment

Mechanochemical synthesis59,63 of nanocrystalline RbSn2F5 was carried out in ZrO2 cups (45 ml) loaded with ZrO2 balls (5 mm diameter) and the corresponding educts. We made use of a high-energy planetary mill (Fritsch Pulverisette 7 premium line) to form the ternary fluoride. To guarantee moisture free reaction conditions the educts (RbF (Sigma Aldrich 99.8%), SnF2 (Sigma Aldrich 99%)) were dried in vacuum over night. Handling of the milling cups, i.e., filling and emptying of the beakers was carried out in an Ar-filled glovebox (H2O and O2 < 0.5 ppm). We milled the starting materials at a rotation speed of 600 rpm for 10 h according to the following procedure: 15 min milling followed by 15 min cooling of the beakers. Subsequently, the powders were annealed at 373, 423 and 473 K for 4 or 8 h in a tube furnace under vacuum or Ar atmosphere. For this annealing step 100 mg of the milled sample was pressed to pellets with a diameter of 5 mm using a hand press and by applying a force of 0.5 tons for 2 minutes. Annealing caused grain growth of the RbSn2F5 crystallites and densified the powder.

The milled and annealed samples were characterised by X-ray diffraction (XRD) under atmospheric pressure and at room temperature. A Bruker D8 Advance diffractometer with Bragg Brentano geometry and CuKα radiation (1.5406 Å) was used to collect the diffractograms. Data points were recorded from 10 to 100° 2θ with a stepsize of 0.02° 2θ; the measuring time for each step was 1 second. Rietveld Refinement was performed with X-PertHighScorePlus (PANalytical).

Magic angle spinning (MAS) NMR was carried out on a Bruker Avance III 500 spectrometer at a nominal magnetic field...
of 11.7 T. This external magnetic field translates in resonance frequencies of 186.40 MHz for \(^{119}\)Sn, 470.30 MHz for \(^{19}\)F and 163.60 MHz for \(^{87}\)Rb. We used a Bruker MAS probe designed for 2.5 mm rotors (ZrO\(_2\)) to acquire free induction decays (FIDs) at a spinning speed of 25 kHz (target gas flow: 400 L h\(^{-1}\), frame cooling: 35% of target gas flow). The bearing gas temperature was 293 K.

Spectra were obtained after Fourier transformation of the FIDs and referenced to the isotropic chemical shifts \(\delta_{\text{iso}}\) of LiF (\(\delta_{\text{iso}}(^{119}\text{Sn}) = -204.3\) ppm), SnO\(_2\) (\(\delta_{\text{iso}}(^{119}\text{Sn}) = -604.3\) ppm) and RbNO\(_3\) (\(\delta_{\text{iso}}(^{87}\text{Rb}) = -30\) ppm site 3), respectively. The relaxation rates \(1/T_{1}\) and \(1/T_{1p}\) were determined with a Bruker Avance III 300 NMR spectrometer at a magnetic field of 7.04 T, i.e., at a \(^{19}\)F NMR resonance frequency of 281.79 MHz. Prior to the relaxation measurements the powder sample was fire-sealed in a glass cylinder with a length of approximately 3 cm and 4 mm in diameter. The rates were recorded with the saturation recovery pulse sequence where at first a train of 10 closely spaced 90° pulses destroys any longitudinal magnetization \(M_z\) before its recovery as a function of delay time \(t_d\) was then detected with a single 90° pulse. The transients \(M_z(t_d)\) were analyzed with stretched exponentials \(M_z(t_d) \propto 1 - \exp (- (t/T_{1p}))\) with \(0 < \gamma \leq 1\). While \(T_1\) NMR is sensitive to fast F anion dynamics, slower motional processes were measured with the spin-lock technique introduced by Slichter and Ailion\(^{64-66}\) utilizing the pulse sequence 90°(\(t_{\text{lock}}\)) – acq.\(^{67-70}\) The locking frequency \(\omega_L\) was set to \(\omega_L/2\pi \approx 100\) kHz and the duration of the locking pulse \(t_{\text{lock}}\) varied from 100 \(\mu\)s to 10 ms. Note that the recycle delay for the spin-lock experiments was at least \(5 \times T_1\) to ensure complete longitudinal relaxation between each scan. Once again, stretched exponentials served to parameterize the spin-lock transients \(M_z(t_{\text{lock}}) \propto \exp (- (t_{\text{lock}}/T_{1p})) (0 < \gamma_p \leq 1)\) to extract \(T_{1p}(1/T)\).

To carry out the impedance spectroscopy measurements, approximately 60 mg of the sample powder was pressed to cylindrical pellets with a final diameter of 5 mm, using a hand press. As for the annealing step, we applied a uniaxial pressure of 0.5 \(t\) for 2 min. Au electrodes, which block ion transport, with a thickness of 100 nm were sputtered onto both sides of the pellets using a Leica sputter device (EM SCD050).

Alternating current (ac) impedance measurement were then performed with a broadband spectrometer (Novocontrol, Concept 80) in combination with an active BDS 1200 cell and a ZGS interface.\(^{21}\) The temperature was varied from 173 K to 473 K controlled by a QUATRO cryosystem. Our conductivity measurements covered a frequency range from \(10^{-2}\) Hz to \(10^{7}\) Hz. All experiments were performed under a constant flow of dry, freshly evaporated \(N_2\) gas. ZView (Princeton Applied Research) and IGOR Pro (WaveMetrics) software were used to analyze the data.

For Hebb–Wagner-type polarisation measurements under \(N_2\) atmosphere we used pellets with 5 mm in diameter and employed a Parstat MC potentiostat (Princeton Applied Research) equipped with a low-current option. All preparation steps, including the metallisation, were carried out in \(Ar\) filled gloveboxes with an \(O_2\) and \(H_2O\) content of less than 1 ppm.

### 3 Results and discussion

#### 3.1 X-ray diffraction

The phase purity of mechanosynthesized \(\text{RbSn}_2\text{F}_5\) before and after the annealing steps was studied by XRD, the corresponding diffractograms are shown in Fig. 2. Directly after milling a diffractogram is obtained that is composed of relatively broad reflections due to both small, nm-sized crystallites and lattice strain. It already resembles that of the low-temperature modification of \(\text{Rb}_2\text{SnF}_5\) showing that the ternary fluoride is directly obtained via this one-pot mechanoc hemical synthesis.

Soft annealing, i.e., holding the sample for 8 h at 473 K under dry, oxygen-free inert gas atmosphere, clearly narrows the reflections because of crystallite growth and/or the release of strain. Lower annealing temperatures also lead to narrow reflections but the narrowing turned out to be less pronounced. Worth noting, if we simply store the ball-milled sample for several month in dry \(Ar\) atmosphere, we recognize a significant growth in average grain size. Therefore, crystallization also takes place under ambient conditions. At his temperature the crystallization kinetics are, of course, much slower than at high \(T\).

![Fig. 2 X-ray diffractograms of all \(\text{RbSn}_2\text{F}_5\) samples prepared. XRD patterns were recorded at room temperature before and after the annealing steps indicated. The vertical bars shows the expected positions of the reflections for the low-\(T\) and high-\(T\) modification, respectively. While the reflections for the phase being stable above 368 K were taken from literature (ICSD no. 247178, recorded at 538 K); those for the low-\(T\) modification were constructed according to the structure model proposed by Yamada et al.\(^{32}\)](image-url)
Obviously, crystal growth is driven by the high F anion conductivity of the samples. For comparison, at 293 K the ionic conductivity $\sigma_{dc}$ is $6.24 \times 10^{-3}$ S cm$^{-1}$, see below.

The final reflections seen after soft annealing are in agreement with the structure refinement proposed by Yamada et al.,$^{32}$ assuming $P\bar{3}$ symmetry and vacancies on the F1, F2 and F3 positions, see also Fig. 1. In Fig. 2 the positions of the main reflections of both the high-$T$ and low-$T$ phase of RbSn$_2$F$_5$ are indicated by vertical lines. We also included a simulation of the XRD pattern of the low-$T$ form of RbSn$_2$F$_5$.

Annealing the samples at temperatures higher than 473 K, e.g., at 568 K for several hours, causes decomposition of the ternary fluoride. Light microscopy revealed small regions that shine metallic. We assume that, due to disproportionation of Sn$^{4+}$, metallic tin is formed at sufficiently high $T$; cf. also Fig. S1 (see ESI†). Scanning electron microscopy showed a mixture of needle-like crystallites and rectangular tubes with a length of up to 20 $\mu$m, see also Fig. S1 (ESI†).

Below 368 K the ternary fluoride crystallizes with $P\bar{3}$ symmetry ($Z = 3$); at higher temperatures RbSn$_2$F$_5$ reversibly transforms to $P\bar{3}$ with $Z = 1$. The same transition has been reported for K$_2$Sn$_5$. Yamada et al. investigated this contraction along the c-axis. The contraction is accompanied by an expansion along the ab-axis.$^{32}$ Defect disorder in the vacancy-rich (F1, F2, F3)-sublattices, caused by the phase transition, leads to an easily measurable increase in F anion conductivity. This increase is also seen here; we used broadband conductivity spectroscopy to study electrical responses over a wide range of temperature and a broad frequency region.

### 3.2 F anion transport in RbSn$_2$F$_5$

Conductivity isotherms of annealed RbSn$_2$F$_5$ are shown in Fig. 3a. If we look at data recorded up to $10^7$ Hz distinct frequency-independent (direct current, dc) plateaus are visible that merge into dispersive regimes. At first glance, these regimes can be approximated with a Jonscher power law, $\sigma' \propto \nu^\kappa$. Here, the exponent turned out to depend only slightly on temperature and amounts to $\kappa \approx 0.6$. While for 3D ionic conductors $\kappa$ usually shows values ranging from 0.65 to 0.85; 2D ionic transport is assumed to be characterized by exponents of approximately 0.55. As pointed out by Sidebottom,$^{72}$ for 1D ion transport even lower values of 0.3 are expected. The latter has recently been found for channel-like ion transport in BaMgF$_4$. Considering $\kappa$ extracted from the fits shown in Fig. 3, the shape of the dispersive regimes provides indications that 2D ion dynamics prevails in RbSn$_2$F$_5$.

We will see later on that this view is supported by diffusion-induced nuclear spin relaxation. It is also in line with earlier reports on 2D ionic conduction in coarse-grained RbSn$_2$F$_5$ investigated by both impedance spectroscopy and NMR.$^{32,58}$

A closer look at the data, especially if we include conductivity data recorded up to the GHz range, reveals that the situation is, however, more complex than can be recognized at first glance. At very low temperatures the isotherms, irrespective if we look at those from micro- or nanocrystalline RbSn$_2$F$_5$ (see Fig. 3a and b) deviate from the $\sigma' \propto \nu^{0.6}$ behaviour. Instead the dispersive regimes merge into a classical nearly constant loss (NCL) regime,$^{72,74}$ being characterized by $\kappa \rightarrow 1$. At sufficiently low $T$ it is thus difficult to separate the two contributions from each other. On the other hand, at high temperatures, i.e., before the phase transformation of RbSn$_2$F$_5$ occurs, we can recognize that $\sigma'$ passes into a second dc plateau at frequencies above $10^9$ Hz, see the arrow in Fig. 3a.

To clarify this feature we extended our measurements to frequencies in the GHz range. Fig. 4 shows the conductivity isotherm recorded at 333 K. It is clearly composed of two dc plateaus, the one occurring at high frequencies definitely belongs to bulk ion dynamics, while the one extending over a large frequency range at lower $\nu$ might also be influenced by grain boundary contributions. Importantly, the dispersive regime of the bulk plateau, whose conductivities obey an Arrhenius law with a very similar activation energy as $\sigma_{dc}$ (see Fig. 3c) (0.52 eV),

![Fig. 3](image-url)
is characterised by $k = 0.54$. This value is even closer to what we expect for 2D ionic conduction.\textsuperscript{72}

The two contributions to the overall electrical response of $\sigma'$ can also be distinguished in the Nyquist plots of Fig. 5, where the imaginary part $-Z''$ of the complex impedance $Z$ is plotted versus its real part $Z'$. The higher the temperature the better the separation; at low $T$ the two semicircles merge into each other. Together with the NCL-type response, showing up at even lower $T$, they cannot be separately analyzed at $T \{ 293 \text{ K}$.\textsuperscript{73}

We analyzed the complex impedance data by using suitable equivalent circuits consisting of individual resistances $R$ and constant phase elements (CPEs) representing the responses from bulk, grain-boundaries (g.b.) and electrodes. The complex impedance $\hat{Z}_{\text{CPE}}$ of a constant phase element can be simply expressed by

$$\hat{Z}_{\text{CPE}} = \frac{1}{(Qj\omega)^n} \quad \text{with} \quad j = \sqrt{-1}$$

(1)

$Q$ has the numerical value of the admittance at $\omega = 1 \text{ rad s}^{-1}$. Thus, the capacitance $C$ of the CPE is given by

$$C = R^{(1-n)/n} Q^{1/n}$$

(2)

Values for $C$ are included in Fig. 5. $C < 10 \text{ pF}$ clearly points to a bulk response the semicircles at high frequencies describe.

\textbf{Fig. 4} (a) Broadband conductivity isotherm (333 K) of microcrystalline RbSn$\text{F}_5$. At low frequencies electrical response is governed by piling up of F anions at the ion-blocking electrodes. This region passes into the first dc plateau whose dispersive region is given by $\sigma' \propto \nu^{1/2}$. Most likely, it is affected by interfacial processes. The second plateau at higher $\nu$ represents bulk ionic dynamics with $\sigma' \propto \nu^{0.95}$ indicating 2D ionic conduction. The inset shows the corresponding permittivity spectrum. (b) temperature dependence of the electrical resistivity ($\rho/\rho_0$) measured for two frequencies. The asymmetric peaks reveal two activation energies characterising long-range ion transport and short-range dynamics.

\textbf{Fig. 5} (a) Nyquist representation of the complex impedance data of microcrystalline RbSn$\text{F}_5$. The depressed semicircle at high frequencies shows bulk ionic dynamics, whereas the electrical response leading to the second one seems to be influenced by interfacial processes. The spike at low $\nu$ originates from polarisation effects. Circles indicted by dashed lines show results from analysing the overall response with appropriate electrical equivalent circuits. Here, we used a parallel combination of three (R-CPE) elements. A complete fit is shown as solid line for the curve measured at 353 K. The values in pF show the capacities obtained from the fits. The inset in (c) shows the polarisation curve that has been measured at 393 K.
As an example, the inset of Fig. 5a shows two semicircles with nearly the same \( R \). Whereas the high-frequency arc, being assigned to the bulk process, is characterized by \( n = 0.74 \), indicating correlated ionic transport, the g.b. semicircle yields \( n = 0.94 \approx 1 \), almost behaving like an ideal RC unit. This result is expected for a grain-boundary electrical response. Finally, we used a polarisation measurement\(^{15}\) to estimate the electronic contribution to the overall conductivity probed by impedance spectroscopy. For this purpose, a pressed \( \text{RbSn}_2\text{F}_5 \) pellet outfitted with ion blocking Au electrodes was used. We applied a potential of 0.2 V and followed the current \( I \) over time \( t \) (see the inset of Fig. 5c). The final current measured at 393 K, i.e., after steady-state conditions had been reached, is in the order of 30 nA and points to an electronic conductivity of \( 1.46 \times 10^{-7} \text{ S cm}^{-1} \). This value is by several orders of magnitude lower than the total conductivity at 393 K (\( 4.3 \times 10^{-3} \text{ S cm}^{-1} \)). Hence, the \( F^+ \) transference number is close to 1 showing that \( \text{RbSn}_2\text{F}_5 \) is a pure ionic conductor.

The two electrical relaxation processes are also seen in permittivity spectra. Whereas isotherms recorded at high \( T \) are less suitable to separate them (see the inset of Fig. 4a), at low \( T \) the real part, \( \varepsilon' \), of the complex permittivity \( \varepsilon \) clearly reveals two contributions, see ESI† (Fig. S2). We attribute these two processes to electrical relaxation in the bulk and caused by g.b. regions. Similar features are also seen for the nanocrystalline sample, for which \( \sigma_{dc} \) almost coincides with that of the annealed sample, see Fig. 3c. In both cases, below 370 K the product \( \sigma_{dc}T \) follows an Arrhenius line characterized by 0.52 eV. This activation energy perfectly agrees with that published by Yamada et al.\(^{1,22}\) and Hirokawa et al.\(^{58}\) both studies report on an activation energy of 0.54 eV.

Almost the same activation energy is obtained if we analyze \( \tan \delta \) peaks (0.48 eV, see Fig. 3c, right axis) or electric modulus peaks \( M'' \) (0.49 eV), not shown here for the sake of brevity. The slight increase from 0.48 eV to 0.52 eV, which is seen when we compare the temperature behaviour of \( \sigma_{dc}T \) with that of \( \nu_{\text{max}} \) from \( \tan \delta \), points to a very slight increase of the charge carrier concentration \( N \) with increasing temperature. For comparison, Yamada et al. reported that \( N \) did not change much with \( T.\(^{12}\)\)

If we look at electrical properties recorded at fixed frequency but variable temperature further information about the energy landscape the \( F \) anions sense can be extracted. In Fig. 4b the temperature dependence of the resistivity, expressed as \( M'/\phi_0 \), is shown for two frequencies, \( \nu = 100 \text{ kHz} \) and \( \nu = 1 \text{ MHz} \). Asymmetric relaxation peaks are obtained with the high-\( T \) flanks yielding 0.56 eV in very good agreement with \( \sigma_{dc}T(1/T) \). Importantly, the low-\( T \) flank is characterized by a much smaller value of approximately 0.2 eV. According to Ngai’s coupling concept of ionic transport,\(^{75–77}\) such values can be identified as the activation barriers characterising short-range ion hopping processes.

### 3.3 Local structures and \( F \) anion diffusivity in \( \text{RbSn}_2\text{F}_5 \) as seen by NMR

\( ^{19}\text{F} \) NMR provides insights into both local structure and dynamics of solids. In Fig. 6 \( ^{19}\text{F} \), \( ^{119}\text{Sn} \) and \( ^{87}\text{Rb} \) MAS NMR spectra are shown, which were recorded to characterize the annealed sample. \( ^{119}\text{Sn} \) MAS NMR, carried out at 25 kHz spinning speed, reveals a single, anisotropically broadened line in agreement with the layered crystal structure. The chemical shift anisotropy turned out to be −1850 ppm. The \( ^{87}\text{Rb} \) NMR spectrum shows a broad resonance at 695 ppm, when referenced to \( \text{SnO}_2 \) (0 ppm). At a spinning speed of 25 kHz we were not able to resolve the two \( \text{Rb} \) positions of \( \text{RbSn}_2\text{F}_5 \). Either they show very similar chemical shifts or (local) structural disorder, even for the annealed sample, leads to a wide distribution of magnetic and quadrupolar electric

**Fig. 6** (a)-(c) \( ^{119}\text{Sn} \), \( ^{87}\text{Rb} \) and \( ^{19}\text{F} \) MAS NMR spectra of microcrystalline \( \text{RbSn}_2\text{F}_5 \), which was obtained by a mechanochemical route with subsequent soft annealing at 473 K. The small intensities at −19 ppm and −25 ppm for \( ^{87}\text{Rb} \) most likely indicates some very minor decomposition products. For comparison, \( \text{RbF} \) is expected to show NMR lines at −19.3 ppm when referenced to \( \text{RbCl} \) (or \( \text{RbNO}_3 \)). The line at −23 ppm might be attributed to \( \text{RbF} \) doped with residual \( \text{Sn} \). Asterisks mark spinning sidebands. See text for further explanation.
interactions causing broad resonances. At low temperatures the
$^{19}$F MAS NMR spectrum reveals several, at least 4, lines with
distinct chemical shifts and intensities (labelled A, B, C and D,
see Fig. 6b). This result is expected when we remember the
various magnetically inequivalent F sites in the structure of
RbSn$_2$F$_5$. With increasing temperature the lines coalesce yielding
a single line (see line C) in the center of gravity of the
spectrum. This line already shows up at 243 K. Thus, even lower
temperatures are needed to completely freeze F anion exchange
in RbSn$_2$F$_5$ illustrating its fast ion dynamics with respect to the
NMR time scale.

Variable-temperature $^{19}$F NMR spectra recorded under static
conditions also reveal this coalescence, see Fig. 7. In the rigid-
lattice regime, which is reached at sufficiently low $T$, we deal with
a dipolarly broadened signal composed of several contributions
as expected from MAS NMR. With increasing $T$ dipole–dipole
interactions are averaged; in the extreme narrowing regime, i.e.,
above 313 K, a single line governs the spectra, once again
showing that nearly all F anions participate in fast self-
diffusion processes. Only the very shallow signal at $-75$ ppm
reveals some F anions that do not contribute to the coalesced
signal, see the arrow in Fig. 7.

Comparing the spectra for microcrystalline RbSn$_2$F$_5$ with
those of nanocrystalline RbSn$_2$F$_5$ we see that heterogeneous
motional narrowing starts at slighter lower $T$ for the nanocrystalline
sample, see Fig. 7. While the ionic conductivity of microcrystalline
and nanocrystalline RbSn$_2$F$_5$ reveals no significant difference,
in defect-rich ball-milled RbSn$_2$F$_5$ (local) structural disorder slightly
increases ionic motion – at least on the length scale to which NMR
line shapes are sensitive. Obviously, the defect structure of nano-
RbSn$_2$F$_5$ is not of detrimental nature for long-range ion transport.
Ions at the grain boundary or interfacial regions might benefit from
such disorder, while those having access to long-range 2D pathways
along the inner surfaces already participate in fast exchange
processes. However, in contrast to other systems the enhance-
ment seen for nanocrystalline RbSn$_2$F$_5$ turned out to be marginal.

For comparison, for poorly conducting oxides with 3D pathways,
the introduction of defects usually leads to an enhancement in
ion dynamics by several orders of magnitude. As an example,
this behaviour has also been observed for nanocrystalline LiNbO$_3$
and LiTaO$_3$ prepared by high-energy ball milling.

Diffusion-induced $^{19}$F NMR spin–lattice relaxation rates $R_{1(o)}$
for both annealed and as-prepared RbSn$_2$F$_5$ are shown in Fig. 8.
Whereas spin–lattice relaxation in the laboratory frame ($R_1$),
i.e., being measured at Larmor frequencies in the MHz range, is
sensitive to short-range F motions on the angstrom scale, with
the rates recorded at locking frequencies in the kHz range ($R_{1(o)}$)
we sense long-range ion transport. Below 220 K the rates $R_1$ are
dominated by non-diffusion induced processes. $^{19}$F spins couple
to phonons or paramagnetic impurities. Above 220 K spin–lattice
relaxation gets increasingly controlled by F motional processes.

The flanks seen in Fig. 8a result in activation energies of ca.
0.25 eV. This value agrees well with those seen on the low-$T$
flank of the $M^2/\omega_0^2$-curves shown in Fig. 4b. As RbSn$_2$F$_5$
reversibly transforms into a different crystal structure at 368 K, the $R_1$
rates show deviations from Arrhenius behaviour at this temperature.
Spin–lattice relaxation in nanocrystalline (ball-milled) RbSn$_2$F$_5$
is faster by approximately 1 order of magnitude if we compare $R_1$
rates measured at 330 K. Obviously, local F dynamics is some-
what faster in the non- annealed form; this increase in local
diffusivity, however, does not affect long-range ion transport in
RbSn$_2$F$_5$ as $\sigma_{dc}$ is the same for the two samples.

The behaviour of $\sigma_{dc}$ is also seen in $R_{1(p)}$. Obviously, $R_{1(p)}$
measurements are able to detect the same long-range ion
dynamics as is sensed by $\sigma_{dc}$. The $R_{1(p)}$ rates of annealed and
non-annealed RbSn$_2$F$_5$ almost coincide and follow the expected
behaviour for a diffusion-induced relaxation processes when
$R_{1(p)}$ is plotted vs. $1/T$. In general, $R_{1(p)}$ (and $R_1$) will pass through a
diffusion-induced rate peak whose maximum shows up when the
jump rate $\tau^{-1}$ reaches the order of the locking (or Larmor)
frequency: $\omega_1(0)\tau^{-1}$. While in the limit $\omega_1 \tau \gg 1$ the flank of the

**Fig. 7** $^{19}$F NMR spectra of microcrystalline and nanocrystalline RbSn$_2$F$_5$
recorded under static conditions and at the temperatures indicated. At
temperatures above 313 K the lines of both samples almost fully coalesce
revealing that nearly all F anion sites participate in ionic diffusion.
Motional narrowing and coalescence turned out to occur at slightly higher $T$
for the annealed sample with less structural disorder. The arrow points to a
narrow tip on top of the dipolarly broad line of as-prepared, nanocrystal-
line RbSn$_2$F$_5$; for this sample changes in line shape show up at slightly
lower temperature than for the sample annealed at 473 K. This difference is
also seen when the spectra recorded at 253 K are compared.
For correlated motion, instead, the low-
T slope being smaller than that in the low-
T regime.

For β = 2, eqn (5) is identical with the result for 3D uncorrelated motion. \( \tau^{-1} \) is expected to be identical with the jump rate \( \tau^{-1} \) within a factor of 2–3. \( \tau^{-1} \) is assumed to be thermally activated according to an Arrhenius law:

\[
\tau^{-1} = \tau_0^{-1} \exp\left(-\frac{E_a}{k_B T}\right)
\]

where \( k_B \) is Boltzmann’s constant, \( \tau_0^{-1} \) represents the pre-factor which usually shows values being in agreement with those expected for phonon frequencies.

Using \( f(\omega_1)^{3D} \), see eqn (3), to analyse the rate peaks of Fig. 8, yields fits that properly agree with the temperature behaviour of the rates measured, see the solid lines in Fig. 8. The activation energies for micro- and nanocrystalline RbSnF₅ turn out to be 0.52 eV and 0.48 eV, respectively. Especially the value for micro-RbSnF₅ perfectly agrees with that from conductivity spectroscopy.

It is valid for homonuclear \(^{19}\text{F–^{19}}\text{F} \) spin fluctuations; here we restricted ourselves to a single term for a good approximation of the rates measured. The limiting cases of eqn (3) for the high- and low-T slopes of the corresponding \( R_{1s}(1/T) \) relaxation peak are the following ones:²²

\[
f(\omega_1)^{3D} \propto \tau_c \ln(1/(2\omega_1\tau_c)), \quad \text{for } \omega_1\tau_c \ll 1
\]

\[
f(\omega_1)^{3D} \propto \tau_c^{-1-\beta}(2\omega_1)^{-\beta}, \quad \text{for } \omega_1\tau_c \gg 1
\]

\( R_{1s}(1/T) \) peak is influenced by correlation effects and structural disorder, the flank in the regime \( \omega_1 T \ll 1 \) should sense dynamic parameters being comparable to long-range ion dynamics. Here, the low-T flanks yield 0.29 eV and 0.24 eV, respectively. Once again, these values agree well with those obtained from \( R_1 \) measurements and the analysis of \( q^2 \). The high-T flank, however, results in 0.39 eV for nano-RbSn₂F₅ and 0.41 eV for micro-RbSn₂F₅. These activation energies are clearly smaller than those seen by conductivity spectroscopy. \( E_a \) extracted from the slope of high-T flanks is only of use when 3D diffusion processes are to be analyzed.

If we take into account 2D diffusion and use the semi-empirical relaxation model introduced by Richards,⁵,⁶,²² to analyze the \( R_{1s}(1/T) \) NMR peaks we obtain a different result. The solid lines in Fig. 8a show fits with spectral density functions \( f(\omega_1)^{2D} \) that include a logarithmic frequency dependence of the \( R_1 \) rates in the limit \( \omega_1 T \ll 1 \). This dependence is characteristic for 2D diffusion.

\[
f(\omega_1)^{2D} \propto \tau_c \ln(1 + (2\omega_1\tau_c)^{\beta}) \propto R_1
\]

Here, \( \tau_c \) denotes the motional correlation time. This spectral density function is based on the BPP-type one, named after Bloembergen, Purcell and Pound, which describes, if \( \beta = 2 \), uncorrelated, isotropic (3D) jump diffusion:

\[
f(\omega_1)^{3D} \propto \tau_c/(1 + (2\omega_1\tau_c)^{\beta})
\]
Here, as mentioned above, we have restricted \( f(\omega_i)^{1D} \) (with \( i = 2, 3 \)) to a single term. Including higher-order terms does not change the quality of the fits and has no effect on \( E_a \) and \( \tau_0^{-1} \).

The pre-factors \( \tau_0^{-1} \) of the fits shown in Fig. 8b are in the order of \( 2 \times 10^{15} \, \text{s}^{-1} \). Such a value is relatively high but in agreement with similar observations for surface diffusion.\(^{83}\) Obviously, F diffusion along the buried or inner planes\(^{84}\) of \( \text{RbSn}_2\text{F}_5 \) resembles ion dynamics on surfaces.

In both cases, i.e., for nanocrystalline and microcrystalline \( \text{RbSn}_2\text{F}_5 \), the correlation factor \( \beta \) turned out to be 1.51 (nano) and 1.57 (micro), respectively. \( \beta \) directly influences the slope on the low-\( T \) side, the smaller value of 1.45 leads to a slightly smaller slope for nano-\( \text{RbSn}_2\text{F}_5 \) as seen in Fig. 8b. Considering the frequency limits of \( f(\omega_i)^{3D} \) (\( \tau_i \approx \tau_c \) and \( \tau_i \approx \tau_c^{-1}/(\omega_0-\omega) \)) we see that the activation energies on the low-\( T \) and high-\( T \) side are connected to each other via

\[
E_a^{\text{low-}T} = (\beta - 1)E_a^{\text{high-}T}
\]

For 2D ionic motion essentially the same equation holds true, we have, however, to replace \( E_a^{\text{high-}T} \) with the activation energy from the fit with \( f(\omega_i)^{1D,2D} \). If we simply take the slope of the \( R_{1}(1/T) \) peak we must consider that \( E_a^{1D} \) is related to \( E_a^{2D} \) via \( E_a^{3D} = 3/4E_a^{2D} \), and with the values obtained here we have 0.39 eV = 3/4 \times 0.52 eV. With \( \beta = 1.57 \) the relationship \( E_a^{2D}(\text{low-}T) = (\beta - 1)E_a^{2D} \) is also fulfilled as we indeed have found 0.29 eV \( \approx 0.57 \times 0.52 \, \text{eV} \). The same also holds for nanocrystalline \( \text{RbSn}_2\text{F}_5 \) with \( \beta = 1 \approx 0.5 \), and \( E_a^{2D}(\text{low-}T) = 1/2E_a^{2D} \).

In summary, while long-range ion transport in microcrystalline \( \text{RbSn}_2\text{F}_5 \) is characterized by 0.52 eV, short-range motions, taking into account correlation effects such as strictly confined hopping processes, local disorder and Coulomb interactions are best described by an activation energy of 0.29 eV. For nanocrystalline \( \text{RbSn}_2\text{F}_5 \) this value is somewhat reduced to 0.24 eV; this slight change is also reflected in \( ^{19}\text{F} \) NMR line narrowing, see above. This view on ion transport is also in agreement with the model introduced by Ngai. Independent of any dimensionality effects in Ngai’s coupling concept dispersive regions in \( \sigma(r) \) would be expected that follow a \( r^{3-\beta-1} \) behaviour, which is fulfilled in the present case.

To further compare results from NMR with those from conductivity spectroscopy, we can use the rate \( R_{1}(1/T) \) peak to estimate a self-diffusion coefficient for \( F^- \) hopping in \( \text{RbSn}_2\text{F}_5 \). At the peak maximum, which is seen at 273 K, the condition \( \tau_c \approx 0.5 \, \text{s} \) is valid; here, we have \( 1/\tau_c = 2.5 \times 10^8 \, \text{s}^{-1} \). Using the Einstein–Smoluchowski equation\(^{85,86}\) \( D = \sigma()^2(2D) \) with \( d = 2 \) for 2D diffusion we obtain \( D = 2.8 \times 10^{-14} \, \text{m}^2 \, \text{s}^{-1} \) if we insert a mean jump distance of \( \alpha = 3 \, \text{Å} \). The jump distances of the F anions labelled F2, F3 and F4 (see Fig. 1) range from 2.89 to 2.97 Å. The distance from F1 to F2 is 2.95 Å. For comparison, at 273 K the bulk ionic conductivity is in the order of \( 1.4 \times 10^{-5} \, \text{S} \, \text{cm}^{-1} \). This value translates, according to the Nernst–Einstein equation\(^{87,88}\) using a carrier charge density of \( 3 \times 10^{27} \, \text{m}^{-3} \), into a solid-state diffusion coefficient \( D_o \) of \( 6.7 \times 10^{-14} \, \text{m}^2 \, \text{s}^{-1} \). Thus, as the two diffusion coefficients only differ by a factor of 2, \( ^{19}\text{F} \) NMR spin–lattice relaxation, if the maximum of the rate peak is used to estimate \( D \), and conductivity spectroscopy sense the same motional process in layer-structured \( \text{RbSn}_2\text{F}_5 \).

Finally, we shall discuss the change in ion dynamics when going from microcrystalline \( \text{RbSn}_2\text{F}_5 \) to its structurally disordered, nanocrystalline form. Many studies, dedicated to comparing diffusion properties of nanocrystalline ceramics with those from coarse-grained materials of the same chemical composition, report on huge differences at least if poorly conducting oxides or fluorides are considered, see above.\(^{77,78,80}\) For materials with rapid ion dynamics from the start, the influence of structural disorder or size effects on ion transport is expected to be moderate or marginal if not without any positive effect on ion transport. If we consider layered materials structural disorder might even slow down ionic transport rather than increase it. For nanocrystalline \( \text{Li}_{x}\text{TiS}_2 \) (\( 0 < x \leq 1 \)), crystallizing with a layered structure, Winter and Heitjans did not find any large increase in Li diffusivity when compared to its coarse-grained form.\(^{89,90}\) Li diffusion in the TiS\(_2\) host is governed by very similar activation energies for the two forms. The incorporation of \( \text{Rb} \) for \( \text{Ba} \) in the fast 2D ionic conductor \( \text{BaSn}_2\text{F}_5 \) increases ionic conductivity;\(^{59}\) most likely aliovalent doping affects, however, the slower interlayer exchange process rather than fast intralayer diffusion.\(^{58,91}\) For the layer-structured form of \( \text{LiBH}_4 \),\(^{27,82}\) crystallizing with hexagonal symmetry and showing 2D diffusion, down-sizing the mean crystallite diameter through ball-milling has only small effect on Li ion conductivity.\(^{26}\) On the other hand, the poorly conducting orthorhombic form of \( \text{LiBH}_4 \) with 3D diffusion, clearly benefits from nanostructuring. In such a sample, NMR relaxation measurements clearly revealed a subset of rapidly diffusing Li ions.\(^{93}\)

Here, the nanocrystalline form of \( \text{RbSn}_2\text{F}_5 \) does not reveal strongly enhanced ion dynamics as compared to the annealed material with sharpened X-ray reflections. Conductivity spectroscopy clearly shows that ionic conductivities are the same for the two morphologies. On the contrary, one might even expect a slight decrease if defects disturb the fast 2D diffusion pathways that are already equipped with a large number fraction of vacant F anion sites. While we cannot recognize any strong effect on long-range ionic transport from conductivity measurements, \( ^{19}\text{F} \) NMR line shapes point to slightly faster ion dynamics in the nanocrystalline form as seen by the motionally averaged line emerging at lower temperatures for non-annealed \( \text{RbSn}_2\text{F}_5 \). Presumably, disordered grain-boundary structures act as hosts for these mobile ions being able to contribute to dipole–dipole averaging already at slightly lower temperatures. This observation is consistent with enhanced \( R_1 \) relaxation rates of nano-\( \text{RbSn}_2\text{F}_5 \) if compared to those of microcrystalline \( \text{RbSn}_2\text{F}_5 \). Moreover, the corresponding activation energy on the low-\( T \) side of the spin-lock NMR peak is reduced from 0.29 eV to 0.24 eV.

Although the effects are small, on the short-range or angstrom length scale we see enhanced dynamics for the as-prepared form. Also magnetic field fluctuations of spatially confined jump processes might contribute to faster relaxation processes communicated to other \( ^{19}\text{F} \) spins via spin-diffusion. At least, the F anions residing near the defect sites do not become trapped.
Such trapping effects could easily explain any decrease in overall ion transport of layer-structured materials.

In other cases, fast localized dynamics are able to trigger through-going macroscopic transport. These dynamic processes might be involved in also causing the huge increase in conductivity seen for the aforementioned nanocrystalline oxides, fluorides and carbonates prepared by milling. Prominent examples include, for example, Li\(_{1-x}\)CoO\(_x\) [X = Ta, Nb],\(^{78,79}\) LiAlO\(_2\),\(^{80}\) BaF\(_2\),\(^{95}\) CaF\(_2\)\(^{17,96,97}\) and Li\(_2\)CO\(_3\)\(^{98}\) as mentioned above. Here, the subtle changes when going from the micro scale to nm-sized crystallites are, however, hardly comparable with the boosts in 3D ionic conductivity seen for the disordered systems. To sum up, for the fast 2D ionic conductor RbSn\(_2\)F\(_5\) site disorder is of limited help to further enhance the already rapid long-range ion transport along the internal or buried interfaces.

4 Conclusions and outlook

Layer-structured RbSn\(_2\)F\(_5\) has been prepared by a one-pot mechanochemical approach in a nanocrystalline form. We softly annealed the as-prepared sample in inert gas atmosphere to obtain microcrystalline RbSn\(_2\)F\(_5\) with a mean crystallite diameter in the \(\mu\)m range. Annealing temperatures have to be adjusted carefully to avoid decomposition of the product. Also storing the as-prepared nanocrystalline material in Ar atmosphere for several months lead to grain growth as seen by sharp X-ray reflections. Obviously, the crystallization behaviour is triggered by fast F\(^-\) diffusion in the ternary fluoride. Indeed, conductivity spectroscopy and \(^{19}\)F NMR relaxation show rapid F ion dynamics.

Careful analysis of both the conductivity isotherms and variable-temperature Nyquist curves, which are composed of bulk and grain boundary regions, revealed indications that F dynamics in RbSn\(_2\)F\(_5\) is of 2D nature. Importantly, only if analyzed with a spectral density formalism which was developed for 2D diffusion the \(^{19}\)F NMR data are consistent with dynamic parameters from conductivity spectroscopy. NMR relaxation measurements point to highly correlated F exchange processes for both the nanocrystalline and microcrystalline form. Local jump processes in micro-RbSn\(_2\)F\(_5\) are to be characterized by an average activation energy as low as 0.24 eV; an even lower value of only 0.16 eV can be inferred from dielectric spectroscopy. An activation energy of 0.52 eV, on the other hand, determines long-range ion transport.

By comparing our results on microcrystalline and nanocrystalline RbSn\(_2\)F\(_5\) we see that structural site disorder does not lead to any drastic enhancement of ion dynamics as it has been recognized for other ionic conductors. Obviously, for layer-structured materials, as it is also known for LiCoO\(_2\) used as cathodes in lithium-ion batteries, the structurally perfect layers guiding the ions along the internal interfaces. This guidance is crucial to ensure long-range ion transport being fast enough that additional disorder does not lead to any further enhancement. Quite the contrary, one might also expect the opposite behaviour. Against this background, it seems worth considering the effect of dimensionality as a design principle for fast ion conductors.

Conflicts of interest

There are no conflicts to declare.

Acknowledgements

Financial support by the Deutsche Forschungsgemeinschaft (DFG Research Unit 1277, grant no. WI 3600 4-1-5-2, WI3600/2-1(4-1) and WI3600/5-2 (SPP 1415)) as well as by the Austrian Federal Ministry of Science, Research and Economy, and the Austrian National Foundation for Research, Technology and Development (Christian Doppler Laboratory of Lithium Batteries: Ageing Effects, Technology and New Materials) is greatly appreciated.

References

1. P. Knauth, Solid State Ionics, 2009, 180, 911.
2. P. Knauth and H. Tallur, J. Am. Ceram. Soc., 2002, 85, 1654.
3. K. Funke, Sci. Technol. Adv. Mater., 2013, 14, 043502.
4. P. Heitjans and S. Indris, J. Phys.: Condens. Matter, 2003, 15, R1257.
5. N. Kamaya, K. Homma, Y. Yamakawa, M. Hirayama, R. Kanno, M. Yonemura, T. Kamiyama, Y. Kato, S. Hama, K. Kawamoto and A. Mitsui, Nat. Mater., 2011, 10, 682.
6. S. Hori, T. Saito, K. Suzuki, M. Hirayama, A. Mitsui, M. Yonemura, H. Iba and R. Kanno, Nat. Energy, 2016, 1, 16303.
7. R. Murugan, V. Thangadurai and W. Weppner, Angew. Chem., Int. Ed., 2007, 46, 7778.
8. V. Epp, O. Gün, H.-J. Deiseroth and M. Wilkening, J. Phys. Chem. Lett., 2013, 4, 2118–2123.
9. A. Hayashi and M. Tatsumisago, Electron. Mater. Lett., 2012, 8, 199.
10. A. Hayashi, K. Noi, A. Sakuda and M. Tatsumisago, Nat. Commun., 2012, 3, 856.
11. S. Narayanan, V. Epp, M. Wilkening and V. Thangadurai, RSC Adv., 2012, 2, 2553.
12. V. Thangadurai, S. Narayanan and D. Pinzaru, Chem. Soc. Rev., 2014, 43, 4714–4727.
13. J. C. Bachman, S. Muy, A. Grimaud, H.-H. Chang, N. Pour, S. F. Lux, O. Paschos, F. Maglia, S. Lupart, P. Lamp, L. Giordano and Y. Shao-Horn, Chem. Rev., 2016, 116, 140–162.
14. J. Lau, R. H. DeBlock, D. M. Butts, D. S. Ashby, C. S. Choi and B. S. Dunn, Adv. Energy Storage Mater., 2018, 8, 1800933.
15. Z. Zhang, Y. Shao, B. Lortsch, Y.-S. Hu, H. Li, J. Janek, L. F. Nazar, C.-W. Nan, J. Maier, M. Armand and L. Chen, Energy Environ. Sci., 2018, 11, 1945–1976.
16. S. Breuer, S. Lunghammer, A. Kiesl and M. Wilkening, J. Mater. Sci., 2018, 53, 13669–13681.
17. A. Düvel, B. Ruprecht, P. Heitjans and M. Wilkening, J. Phys. Chem. C, 2011, 115, 23784–23789.
18. C. Rongeot, M. Reddy, R. Witter and M. Fichtner, J. Phys. Chem. C, 2013, 117, 4943–4950.
19. C. Rongeot, M. Anji Reddy, R. Witter and M. Fichtner, ACS Appl. Mater. Interfaces, 2014, 6, 2103–2110.
20. F. Preishuber-Pflugl, P. Bottke, V. Pregartner, B. Bitschnau and M. Wilkening, Phys. Chem. Chem. Phys., 2014, 16, 9580–9590.
80 D. Wohlmuth, V. Epp, P. Bottke, I. Hanzu, B. Bitschnau, I. Letofsky-Papst, M. Kriechbaum, H. Amenitsch, F. Hofer and M. Wilkening, *J. Mater. Chem. A*, 2014, 2, 20295–20306.

81 N. Bloembergen, E. M. Purcell and R. V. Pound, *Phys. Rev.*, 1948, 73, 679.

82 M. Uitz, V. Epp, P. Bottke and M. Wilkening, *J. Electroceram.*, 2017, 38, 142–156.

83 J. Hinterberg, A. Adams, B. Blümich, P. Heitjans, S. Kim, Z. A. Munir and M. Martin, *Phys. Chem. Chem. Phys.*, 2013, 15, 19825–19830.

84 P. Heitjans and M. Wilkening, *Mater. Res. Bull.*, 2009, 34, 915.

85 A. Einstein, *Ann. Phys.*, 1905, 14, 182–193.

86 M. von Smoluchowski, *Ann. Phys.*, 1906, 326, 756–780.

87 R. McKee, *Solid State Ionics*, 1981, 5, 133–136.

88 H. Mehrer, *Diffusion in Solids.*, Springer, Berlin, 2006.

89 R. Winter and P. Heitjans, *J. Phys. Chem. B*, 2001, 105, 6108.

90 R. Winter and P. Heitjans, *J. Non-Cryst. Solids*, 2001, 293, 19.

91 M. Wilkening, A. Düvel, F. Preishuber-Pflügl, K. Da Silva, S. Breuer, V. Šepelák and P. Heitjans, *Z. Kristallogr. – Cryst. Mater.*, 2017, 232, 107–127.

92 V. Epp and M. Wilkening, *ChemPhysChem*, 2013, 14, 3706–3713.

93 S. Breuer, M. Uitz and H. M. R. Wilkening, *J. Phys. Chem. Lett.*, 2018, 9, 2093–2097.

94 D. Prutsch, S. Breuer, M. Uitz, P. Bottke, J. Langer, S. Lunghammer, M. Philipp, P. Posch, V. Pregartner, B. Stanje, A. Dunst, D. Wohlmuth, H. Brandstätter, W. Schmidt, V. Epp, A. Chadwick, I. Hanzu and M. Wilkening, *Z. Phys. Chem.*, 2017, 231, 1361–1405.

95 B. Ruprecht, M. Wilkening, R. Uecker and P. Heitjans, *Phys. Chem. Chem. Phys.*, 2012, 14, 11974.

96 W. Puin, S. Rodewald, R. Ramlau, P. Heitjans and J. Maier, *Solid State Ionics*, 2000, 131, 159–164.

97 W. Puin and P. Heitjans, *Nanostruct. Mater.*, 1995, 6, 885–888.