Inverse method to determine fatigue properties of materials by combining cyclic indentation and numerical simulation

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Abstract: The application of instrumented indentation to assess material properties like Young’s modulus and micro-hardness has become a standard method. In recent developments, indentation experiments and simulations have been combined to inverse methods, from which further material parameters as yield strength, work hardening rate, and tensile strength can be determined. In this work, an inverse method is introduced by which material parameters for cyclic plasticity, i.e. kinematic hardening parameters, can be determined. To accomplish this, cyclic Vickers indentation experiments are combined with finite element simulations of the indentation with unknown material properties, which are then determined by inverse analysis. To validate the proposed method, these parameters are subsequently applied to predict the uniaxial stress-strain response of a material with success. The method has been validated successfully for a quenched and tempered martensitic steel and for technically pure copper, where an excellent agreement between measured and predicted cyclic stress-strain-curves has been achieved. Hence, the proposed inverse method based on cyclic nanoindentation, as a quasi-non-destructive method, could complement or even substitute the resource-intensive conventional fatigue testing in the future for some applications.

Keywords: Cyclic indentation, Vickers hardness, inverse analysis, numerical simulations, cyclic material properties, fatigue life

1. Introduction

Depth-sensing indentations or instrumented indentations are very useful means to characterize and determine mechanical properties (i.e. Young’s modulus and hardness) of thin films as well as of bulk materials [1–5]. Hyung [6] and Suresch et al. [7], [8] have proposed two novel methods to identify the elastic modulus, yield strength, and the hardening exponent through nano-indentation. In addition to this, instrumented indentation experiments make it possible to determine further material properties, such as the strain hardening coefficient and yield strength [9]. Schmaling and Hartmaier [10] have introduced a method to identify plastic material properties (i.e. yield strength and work hardening rate) by using an inverse analysis for the remaining imprint after indentation. A comprehensive comparison of the hardness measurement approaches at diverse scales (i.e. nano, micro, and macro) by Brinell, Vickers, Meyer, Rockwell, Shore, IHRD, Knoop, and Buchholz at was performed by Broitman [11]. He has not only enlightened each indentation method but has also presented its inadequacies in evaluating results. Furthermore, he has discussed the effect of elasticity, plasticity, pileup, sink-in, grain size, and indentation size effects on determining hardness by means of depth-sensing indentation techniques at the micro- and the nanoscale.

The applications of instrumented nanoindentation is not limited to the identification of conventional material properties, such as elastic modulus and hardness; the ease to perform it, also
have attracted the attention of some authors who have employed it to estimate complex material properties like fatigue life or even the famous S-N (Wöhler) curve [12–14]. These quantities need tedious and difficult conventional fatigue experiments; consequently, there are some analytical relationships available to determine the S-N curve and fatigue strength using indentation hardness. For example, the Strzelecki model [12] has described the relationship between fatigue life and material hardness. Similarly, by utilizing the Murakami [13] formulation, Bandara [14] has recommended a full range S-N curve for six different medium steel grades. However, this suggested formulation is material-specific and requires two input parameters, i.e. Vickers hardness and ultimate tensile strength. Furthermore, Bandara [15] has used the Brinell hardness value in order to determine material fatigue strength. The three [12], [14], [15] aforementioned analytical approaches (mainly dependent on the hardness value of the material) have been comprehensively summarized by Strzelecki and Tomaszewski in [16], where they have expounded the merits and demerits of each individual approach and concluded that both models are good to predict tensile strength and yield strength while the Strzelecki model [12] is superior in the prediction of fatigue life as compared to the Bandara model [14], [15].

In classical indentation experiments, only single loading and unloading on the specimen is performed for determining the desired mechanical properties. However, to study the fatigue life in materials, the cyclic indentation has gotten the attention of many authors [17–20]. For example, Lyamkin et al. [17] have shown the potential of cyclic indentation for studying the fatigue properties. As the cycles of indentations are repeated at the same location, therefore, the elastoplastic area of high cyclic indentation demonstrates fatigue under these conditions. For instance, a nano-impact fatigue test is studied by Faisal et al. [18] by using cyclic indentation, and they have concluded that the indenter geometrical shape (Berkovich or conical) and the indentation loading history are crucial in inducing film failure. Moreover, Haghshenas et al. [19] have employed cyclic nano-indentation in order to determine the indentation size effects and the strain rate sensitivity for tantalum. Similarly, Prakash [20] has demonstrated fatigue damage in materials with the help of two different non-destructive techniques, of which one is spherical cyclic indentation. In addition, he has investigated fatigue properties with a cyclic small punch test and with cyclic automated ball indentation and has concluded that the stiffness in the weld region drops more quickly in comparison to the base metal [21]. Xu et al. [22] performed the numerical analyses of flat cylindrical indentation for polycrystalline copper. They have concluded that strain accumulation reached a steady-state indentation depth rate in sinusoidal cyclic loading just like in real fatigue experiments.

From this literature review, it is concluded that using instrumented indentation for determining the fatigue life of materials would reveal significant advantages of indentation testing (quasi-non-destructive technique, less time and cost intensive) over conventional fatigue experiments. Some analytical relations are indeed available to predict the S-N curve for fatigue life based on the hardness value, but these methods are mostly limited to steels and not applicable to softer materials, for instance, copper. Furthermore, it is not possible to analyze the microstructural influences. Hence, there is a need for a more general approach, which could be applied to a larger range of materials. In addition to this, a method, which uses the indentation experimental data for predicting complete uniaxial stress-strain hysteresis, is still missing in the literature according to the author’s knowledge. Yet, this uniaxial stress-strain hysteresis has a key role in fatigue life determination, for which some attempts have already been made as discussed earlier, but the literature still lacks a hybrid method, which predicts the material fatigue life and the complete uniaxial stress-strain hysteresis with a combination of the numerical analysis and Vickers indentation.

2. Material and experiment

2.1 Materials specifications

In this study, we have used a conventional quenched and tempered martensitic high-strength steel SAE 4150 (German denomination 50CrMo4), which exhibits a hardness of 38 HRC. The cyclic
properties of this material have been analyzed in detail by Schäfer et al. [23]. The second material used in this study, technically pure copper, is a conventional Cu-ETP (Electrolytic Tough-Pitch).

2.2 Indentation and fatigue testing

Indentation testing was performed by using a small Zwick™ load indenter and was adapted from Kramer et al. [24]. The test was performed in a cyclic fashion; therefore, the indenter tip was repeatedly indented at the same spot. To hold the sample in the testing position, a constant minimal load remained between the cycles. A minimum load of 2 N and a maximum load of 50 N was used for martensitic steel. Further experiments were also performed for higher forces, i.e. at 75 N and at 100 N as well as for higher hardness such as 47 HRC at 50 N. In addition, indentation was performed for Cu with a maximum load of 10 N and a minimum load of 1 N. The load increased at a rate of 5 N/s. As an example of indentation testing, only the first complete cycle for 50CrMo4 and Cu is demonstrated in Figure 1(a & c). Fatigue experimental data of uniaxial cyclic stress-strain curves are obtained from the study of Schäfer et al. [23], and the details of the experiments are described in his study. Similarly, stress-strain hystereses are shown for the aforementioned two materials (50CrMo4 and Cu) in Figure 1(b & d).

The complete cycle of the indentation test for martensitic steel (50CrMo4) is demonstrated in Figure 2 with three different colors. The first, blue part of the curve indicates the loading, the green section displays the unloading, and the red portion demonstrates the reloading for the force-displacement. It can be seen that the portion of the unloading and reloading makes a closed curve, which is named as force-displacement loop (FD loop) and the intersection point is named as ΔF, in this study. This loop will be used as a target curve for the parameter identification in the following section.

![Figure 1: Experimental results for Cu and 50CrMo4: a) Indentation cycle at 50 N for 50CrMo4 b) Stress-strain from fatigue experiments of 50CrMo4 c) Indentation cycle at 10 N for Cu d) Stress-strain from fatigue experiments of Cu.](image-url)
Figure 2: Force displacement curve from the cyclic indentation curve. Components of the cycle are shown in different colors for clarity.

2.3 Numerical models

The finite element model used in the investigation is depicted in Figure 3a. The indenter is modeled as a rigid body. The specimen is fixed from the bottom, and a vertical load is applied at the center by using a Vickers indenter (DIN EN ISO 6507-2: 2005). For example, the applied force amplitude of 50 N in the simulation is explained as follows. The specimen is indented with the pre-selected applied force amplitude (i.e. 50 N), which is unloaded until the force of approximately 2 N and reloaded to the maximum force (Figure 2). Similarly, the simulations have been run at other indentation force amplitudes of 25 N, 75 N and 100 N. The force-time history from the experiments is used as an input for the simulations so that the loading in experiments can be fully depicted in the simulations.

It is our goal to identify the material parameters, which requires to perform many simulations, and makes it computationally very costly. Therefore, the size of the simulation model (2 mm × 2 mm and extruded to 1.5 mm) is optimized with a mesh size of 4 µm (Figure 3b), and after the mesh convergence study, C3D8 linear elements with a full integration scheme have been chosen in this paper. The friction effect between the indenter and the specimen is also studied, which did not show a considerable effect on the simulation results in the scope of this work.

Figure 3: Details of the Numerical model used. (a): Specimen is held fixed from the bottom and the indenter is placed in the center of the specimen that moves in and out during loading and unloading respectively. (b): The fine meshing is performed at the center of the specimen.

2.4 Material model

In this investigation, the Chaboche material model is used, because it is one of the most efficient and convenient constitutive models incorporating the cyclic plasticity behavior of materials during cyclic loading. Furthermore, the ratcheting behavior of the material, which rises under cyclic loading, can also be analyzed with it. Details of this model for J2 plasticity are given in the subsequent section.
According to the von Mises yielding criterion [26], the yielding of material starts once the second deviatoric stress invariant J2 reaches a critical value. The common formula of this yielding criterion \( f \) is distinct as

\[
f = \sqrt{\frac{3}{2}} \left( \mathbf{S} - \mathbf{k} \right) : \left( \mathbf{S} - \mathbf{k} \right) - (\sigma_0 + R),
\]

where \( \sigma_0, \alpha, S \) represents the initial yield stress, backstress, and deviatoric stress, and where \( R \) represents the isotropic hardening (i.e. constant growth of yield surface) [27]. The increase in plastic strain with respect to the gradient of the yield surface will lead to the definition of the associative flow rule used in this study.

\[
R = Q(1 - e^{-b \varepsilon_{eq}}),
\]

where, \( \varepsilon_{eq} \) is the equivalent plastic strain, \( b \) determines the rate of isotropic hardening, and \( Q \) is the maximum change in the size of the yield surface [29].

In order to model the cyclic behavior of materials, a nonlinear kinematic hardening model was proposed by Armstrong and Frederick [30]. This kinematic hardening model contains only one backstress term (\( \alpha \)) and was extended by Chaboche by decomposing the single backstress term into several backstress terms, making the Chaboche material model [28] capable of capturing the complex kinematic hardening behavior.

The decomposed backstress terms of Chaboche kinematic hardening [28] model are described in the following equation as

\[
\alpha = \sum_{i=1}^{n} \alpha_i; \quad d\alpha_i = \frac{2}{3} C_i d\varepsilon_p - \gamma_i \alpha_i d\varepsilon_{eq},
\]

where \( \gamma_i \) describes the reduction rate of the related modulus with respect to the plastic strain \( d\varepsilon_p \), while \( C_i \) represents the kinematic hardening moduli. The change in the yield surface of the combined hardening evolution for monotonic tension and in the stress space is graphically presented in Figure 4 [27].

![Figure 4: Graphical depiction of the combined hardening growth in the (a) stress space shown by the yield surface and (b) under monotonic tension presented as a stress-strain diagram, after [28].](image-url)
3. Inverse parameter identification

In order to capture the experimental force-displacement curve by simulation, the commercially available LS-Opt optimizer [32] is used. The inverse identification technique is applied, and the schematic of the optimization process is presented in Figure 5. The quality of fit between the simulated and the experimental force-displacement loops is evaluated by using the normalized mean square error (NMSE) as

\[
\text{NMSE} = \frac{1}{N} \sum_{i} \frac{(E_i - S_i)}{E_S},
\]

where \( \bar{E} \) and \( \bar{S} \) represents the average of the experimental \( E_i \) and simulation \( S_i \) values, respectively and \( N \) is the total number of data points. To identify the force-displacement curve, the value of this NMSE is used as an objective function that minimizes the difference between the experimental and simulated force-displacement loops.

Figure 5: Optimization loop used to identify the material parameters by fitting the experimental curve with the simulation curve.

The force-displacement loop as shown in Figure 2 is used as an objective curve to identify the material parameters. For determining material parameters, which meets the given objective (i.e. to minimize the value of NMSE), a genetic algorithm [33] is used because it is a global optimizer. This algorithm generates the first iteration, which contains certain material parameters sets for the identification process. The force-displacement curve from the simulation is taken out using a post-processing script written in Python 3. Based on the fitness results obtained at the end of the first iteration, the algorithm generates the second iteration and the loop continues. In each iteration, the algorithm calculates the fitness of the obtained curve with the experimental force-displacement curve by using NMSE. This loop continues until the convergence criterion (i.e. \( \text{NMSE} = 1 \times 10^{-5} \)) is met or the maximum allowed iterations are reached. The yield stress and Young's modulus are kept constant at 1060 MPa and 204 GPa respectively, based on monotonic stress-strain experimental data.

4. Results and Discussion

4.1 Method development

The experimental force-displacement loop of one complete cycle of indentations is used as a target curve along with \( \Delta F \). The material parameters (see Table 1) obtained after the optimization with this strategy show a good agreement for the complete indentation cycle: The normalized mean square error (NMSE) between the simulated force-displacement loop and the experimental force-displacement loop is \( 2.0 \times 10^{-5} \).

To achieve a comparison with experimentally determined hysteresis from fatigue tests, the hysteresis under a tensile-compressive load is predicted in the next step by using the parameters from
Table 1. Comparing this prediction to the experimental results reveals, with a plastic work error of 2.5 %, a quite good accuracy as can be seen in Figure 6. In the scope of this study, the identified material parameters of cyclic macro-indentation are used to predict the complete uniaxial stress-strain hysteresis for the first time.

![Figure 6](image)

**Figure 6:** (a) Complete cycle of the force-displacement curve from indentation with NMSE = $2.0 \times 10^{-5}$

b) Predicted uniaxial stress-strain hysteresis with a plastic work error of 2.5 %.

There is a clear relationship between the $\Delta F$ value measured by cyclic indentation and the uniaxial stress-strain hysteresis. This relationship is qualitatively investigated in this study. In Figure 7, the results of two objective functions can be seen. “Objective function 1” includes only the curve matching (which minimizes the area difference between experimental and simulated curves) while “objective function 2” considers the value of $\Delta F$ along with the curve matching.

Table 1: Identified material parameters for 50CrMo4 (38HRC) after fitting of force-displacement at 50N

| Symbol | Value |
|--------|-------|
| $C_1$ (MPa) | 262,197 |
| $\gamma_1$ | 373 |
| $C_2$ (MPa) | 4,714 |
| $\gamma_2$ | 0.25 |
| Q (MPa) | -575 |
| b | 262 |

Although, by using the “objective function 1”, the comparison of force-displacement curves from simulation and experiment seems to be in an acceptable range (see Figure 7, solid blue FD loop) having NMSE $3.0 \times 10^{-5}$, nevertheless, the value of $\Delta F$ from the simulation is lower than the experimental $\Delta F$, which has a direct impact on the uniaxial stress-strain hysteresis prediction. The inclusion of the $\Delta F$ into “objective function 2” leads to a better prediction of the uniaxial stress-strain hysteresis as is shown by the dotted blue line hysteresis in Figure 7.
Figure 7: Effect of $\Delta F$ on the uniaxial stress-strain hysteresis prediction (solid blue FD loop displays the fitting of FD loop to the blue experimental FD loop by using objective function 1, while the dotted solid stress-strain hysteresis is the prediction of stress-strain hysteresis. Similarly, the dotted blue FD loop shows the fitting of the FD loop by using objective function 2, while the dotted blue stress-strain hysteresis represents the prediction of the stress-strain hysteresis).

It can be observed that if the $\Delta F$ (from simulation) has a lower value as compared to the experimental $\Delta F$ value, the prediction of the uniaxial stress-strain hysteresis reveals a larger disagreement (plastic work error = 20%) between the experimental and the simulation stress-strain hysteresis. On the other hand, when the value of $\Delta F$ is comparable to the experimental $\Delta F$ value, the uniaxial stress-strain hysteresis provides an acceptable prediction (plastic work error = 2.0%) as demonstrated by the dotted solid curve in Figure 7.

From now on, we will only present the results obtained by “objective function 2” after optimization. As the Chaboche material model is also capable to capture the ratcheting behavior in cyclic loading, further simulations are performed with multiple cycles of indentation to compare the experimental ratcheting effect of force-displacement by using the identified parameters from the complete indentation cycle. The ratcheting observed in simulation and experiment is slightly overestimated. In Figure 8b, force-displacement curves for 13 consecutive cycles are compared with the experiment.

Figure 8: Validation at higher force amplitudes: (a) Predicted force-displacement at 75N (b) Predicted force-displacement at 100N

4.2 Validation

The material parameters, which have been identified at a 50N force amplitude, are also tested at higher forces of 75N and 100N to check the validity of the obtained parameters.
The validation of the method at higher force amplitudes are also in a good agreement as shown in Figure 8a and Figure 8b at the 75N force amplitude (NMSE = 3.3×10⁻⁴) and 100N force amplitude (NMSE = 1.6×10⁻⁴), respectively. Figure 10a demonstrates the comparison of experimental and simulation uniaxial stress-strain hysteresis for the 10th cycle of the same material. The red hysteresis, which is obtained by using the above-obtained fitted material parameters from the cyclic indentation force-displacement curve, shows a quite good agreement (plastic work error = 3.5%) with the experimental hysteresis. Figure 10b demonstrates the maximum and minimum stress on the vertical axis while the horizontal axis displays the cycle number.

It is evident from Figure 10 that the material parameters obtained from the cyclic indentation force-displacement curve can predict higher uniaxial stress-strain hysteresis very accurately, and the difference is less than 4%. This uniaxial stress-strain hysteresis is obtained without any initial input from uniaxial stress-strain hysteresis. The uniaxial stress-strain hysteresis has a key role in determining material fatigue life. As already mentioned, performing fatigue experiments is quite expensive both in terms of cost and time, and performing indentation tests is quite easy and requires fewer resources. By using this technique of identifying kinematic hardening material parameters, the need to perform fatigue experiments will be required only for the validation process.

4.3 Transferability of the method

4.3.1 Transferability to higher force amplitude (75N)
Until now, we have used a 50N indentation force amplitude for identifying material parameters and then predicted the uniaxial stress-strain hysteresis by using these identified parameters. To check the robustness and transferability of our method, we have decided to also fit the 75N indentation curve and to try to predict the uniaxial stress-strain hysteresis by using these parameters. The rest of the optimization setting and procedure were kept the same as explained before. Figure 11a displays the comparison of the cyclic force-displacement curve, while Figure 11b demonstrates the comparison of the uniaxial stress-strain between simulation and experiment. The results are in good agreement (NMSE = 4.0×10⁻⁵) between the experimental and the simulation curve for both force-displacement and uniaxial stress-strain hysteresis. The parameters obtained after the simulation are reported in Table 2 and not so much different from the parameters obtained for the 50N force amplitude.

![Graphs showing force-displacement and stress-strain comparisons](image-url)

**Figure 11**: Transferability of method: a) Indentation of 39HRC at 75N b) Prediction of stress-strain hysteresis of 39HRC.

**Table 2**: Identified material parameters for 50CrMo4 (38HRC) at after fitting of force-displacement 75N

| Symbol   | Value  |
|----------|--------|
| C₁ (MPa) | 257,503|
| γ₁       | 354    |
| C₂ (MPa) | 3,663  |
| γ₂       | 0.2837 |
| Q (MPa)  | -611   |
| b        | 163    |

4.3.2 Transferability to higher hardness (47HRC)

Similarly, the force-displacement at 50N for 47HRC hardness is fitted. The values of yield strength (1400 MPa) is used that is obtained from the monotonic loading experiments. The results of the force-displacement curve after the optimization show a good agreement between the experimental and simulation curve. The prediction of the uniaxial stress-strain curve also depicts a sufficient agreement between simulation and experiment. The difference in energy dissipation between experiment and the prediction is 4.5%.
4.3.3 Transferability for other material (Cu)

The extensive study of using different force amplitudes and different hardness has been done with our method for martensitic steel in the previous section. In this section, the aim is to test our methodology for some other metallic material. For this purpose, copper (Cu), a relatively softer material is selected, and therefore, instead of using a 50N force amplitude, a smaller force amplitude of 10N applied for cyclic indentation. The optimization is performed by using the same setup with two backstress terms (Table 4), and the results after optimization are shown in Figure 13. Figure 13a demonstrates the comparison of the force-displacement at 10N between simulation and experiment, while Figure 13b shows the predicted uniaxial stress-strain at 1% total strain amplitude. It can be seen from Figure 13a that the force-displacement has quite a good fit after optimization. The same is true when we predict the uniaxial stress-strain hysteresis by using these identified parameters and compare it with the experimental uniaxial stress-strain hysteresis. The difference between dissipated energy and predicted stress-strain hysteresis and experimental is only 3.5%.

**Table 3**: Identified material parameters for 50CrMo4 (47HRC) after fitting of force-displacement at 50N.

| Symbol | Value  |
|--------|--------|
| $C_1$ (MPa) | 337,885 |
| $\gamma_1$ | 374 |
| $C_2$ (MPa) | 6,681 |
| $\gamma_2$ | 2.3 |
| $Q$ (MPa) | -724 |
| $b$ | 273 |

**Figure 12**: Transferability of method: a) Fitted indentation force-displacement at 50N for 47HRC b) Prediction of uniaxial stress-strain hysteresis of 47 HRC

**Figure 13**: Transferability of method: a) Fitted indentation force-displacement of Cu at 10N b) Prediction of uniaxial stress-strain hysteresis
Table 4: Identified material parameters for Cu at 10N

| Symbol | Value   |
|--------|---------|
| C₁ (MPa) | 154,790 |
| γ₁     | 2,257   |
| C₂ (MPa) | 11,586  |
| γ₂     | 82      |
| Q (MPa)  | -12     |
| b       | 47      |

5. Conclusions

A novel hybrid method for the inverse analysis of fatigue properties of metals has been introduced. The method combines cyclic Vickers indentation experiments and finite element simulations in an inverse method, by which the material parameters are determined in an iterative way by an optimization scheme. It has been demonstrated that this method can be used to determine the parameters of the Chaboche model for kinematic hardening. Based on these parameters, the model has been employed successfully to predict the cyclic stress-strain responses of a tempered martensitic steel SAE 4150 (German denomination 50CrMo4), with different heat treatments and of technically pure copper. The error in the parameters determined with the inverse method has been evaluated to a value of less than 4% on average. It has been observed that the difference between the maximum and minimum force of the force-displacement loop obtained from cyclic indentation has a direct correlation with the stress amplitude of the hysteresis loop measured in strain-controlled uniaxial fatigue tests, and thus, plays a crucial role in predicting the uniaxial stress-strain hysteresis accurately. By applying the method to high-strength martensitic steel, on which it has been validated for different maximum forces, and also to technically pure copper, its validity has been demonstrated for a wide variety of materials and process parameters. The prediction of a complete cyclic stress-strain curve by using data from cyclic indentation has a great potential to reduce time and cost-intensive fatigue experiments and can thus open a new and economic way to predict the fatigue life of materials with a quasi-non-destructive test method.

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