Maintenance Action Recommendation Using Collaborative Filtering

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ABSTRACT

The problem we were trying to solve in 2013 PHM Society Conference Data Challenge competition is closely related to remote monitoring and diagnostics in industrial applications. This data was generated from an industrial piece of equipment with a sensor network to measure several parameters and an onboard condition monitoring system. The measured data goes through a control logic in order to monitor the equipment’s operating regime. At any time instant when some of these parameters meet a specific condition, the control system generates an unique event id/code. Each case is described by a set of event codes which characterize the atypical operating condition of the equipment. Some of these cases with specific event code combinations may be operationally significant and could be indicative of “Problem Types”, some of which are assumed to be known to the subject matter experts. As a response to these problems, domain experts recommend appropriate diagnostic measures (or maintenance actions) depending on the problem types. The goal of this data competition is to build an automated system that can recommend particular maintenance action(s) to mitigate these problem(s).

1. RECOMMENDER SYSTEMS

Though active research has been conducted in recommender systems for the last two decades, more recently this field has gained tremendous attention particularly in service industry. In simple terms the intention of building recommender systems is to effectively suggest users on possible items of interest with some prior understanding of the contextual information on that user’s and/or similar user’s and/or similar item’s profile. The recommended item(s) is the one with highest estimated “utility metric” that best represents user’s notion of interest. Such “utility metric” include user’s rating expressed explicitly in terms of symbols (stars) or numbers (binary, categorical). In more formal terms, the objective is to maximize user’s utility function ($F_u$) in the joint user-item space ($U \times C \rightarrow \mathbb{R}$) defined by a set of $U$ users where any user $u \in U$ and a set of $C$ items/commodities where any item $c \in C$. The recommender system’s goal is to propose a new item $c^* \in C$ to the user $u$, such that $F_u(c, u)$ is maximized over all $c \in C$.

In this paper we have demonstrated the application of collaborative filtering technique to recommend maintenance actions. However, first we will provide a comprehensive overview on some of the popular recommendation techniques. Based on the literature (Koren & Bell, 2011; Koren, Bell, & Volinsky, 2009; Adomavicius & Tuzhilin, 2005), recommender systems are broadly classified into three groups, namely content filtering, collaborative filtering and hybrid approach which is essentially a combination of collaborative and content filtering. Here filtering is synonymous to estimating $F_u(c, u)$ using either item’s content based features e.g., keyword weights or user’s explicit feedback on items e.g., ratings. In a loose sense, content filtering based approach uses low level information whereas collaborative filtering uses high level information to accomplish the job. Content filtering assumes access to item’s content ($D_c$). In this approach the first step is content based information retrieval where a set of attributes/features ($A_c$) that best describes an item $c$ are extracted. This is followed by estimating $F_u(c, u)$ based on the extracted features of items. We will elaborate this with an example. In the aviation safety domain, suppose an aviation safety officer (end user) is interested in reading a particular class of text reports written by the flight crew/passengers, for example turbulence related reports, then our goal is to recommend the safety inspector with similar reports on turbulence related topic based on his/her preference. In order to do that, we first need to know what are the important keywords that best describes turbulence related topic, e.g., “mountain”, “clear-air”, “convective” etc. There are several approaches in retrieving such information (keywords) and the choice of the approach typically depends on the nature of the data. For example, if we intend to find the keywords from a corpus of (only) turbulence related documents, we may use “Term Frequency-Inverse Document Frequency (TFIDF)” to measure the importance of the words across of the whole corpus. We will provide further details on TFIDF in another section. However if the document corpus contains various topics (e.g.,
weather, maintenance, turbulence, mechanical failure etc.) in varying proportions, then a complex machinery like “Latent Dirichlet Allocation (LDA)” is required to obtain a set of keywords to describe each topic. We refer the reader to the paper (Blei, Ng, & Jordan, 2003) for further details as it is beyond the scope of this paper. Once we obtain the key features (A_c) then the remaining task is to adopt a heuristics or a model based approach to compute the score of the utility function F_u(A_c,D_c) over all new items’ content D_c. The item with the highest score or the n top scoring items are recommended to the user. In the above example, the contents of new reports that closely match the description of turbulence related topic are presented to the safety officer.

As mentioned earlier collaborative filtering based approach does not assume access to item’s content D_c, instead it expects user’s explicit feedback (ratings r_{uc}) on items i.e. user-item interactions (Y_{uc}). One can think of Y_{uc} as a matrix whose rows represent the set of users u_c ∈ U who have provided ratings on a subset of items c ∈ C and the columns represent the set of items, each of which has been at least rated by one or more users. Since users generally provide feedback not necessarily on every items but a small subset of items, Y_{uc} tends to be extremely sparse. In collaborative filtering a new item is recommended to a user u_k based on the ratings of other users u_j having similar taste. In heuristics based collaborative filtering we first retrieve neighboring users u_j and u_k and then use an aggregate function to compute an average rating for each item from c. The item with maximum weight (in this case rating) is recommended to user u_k. The readers are advised to consult the following literatures (Koren & Bell, 2011; Koren et al., 2009; Adomavicius & Tuzhilin, 2005) for detailed description of variations on aggregation functions.

Model based collaborative filtering however relies on mapping the user-item interaction to a latent space to achieve this goal using techniques like matrix factorization (Hoyer, 2002; Wold, Esbensen, & Geladi, 1987; Hoyer, 2004; Lee & Seung, 2001; Berry, Browne, Langville, Paucu, & Plemmons, 2006; Su & Khoshgoftaar, 2009; Cichocki & Zdunek, 2007; Koren & Bell, 2011; Koren et al., 2009), probabilistic mixture model (Condilff, Lewis, & Madigan, 1999) etc. In this paper we will restrict our discussion to matrix factorization methods only. In general matrix factorization methods are easy to understand and interpret from a mathematical perspective and also flexible in many sense. We will elaborate on some of these advantages. In these techniques we represent the user-item interaction Y_{uc} as a product of two entities, one representing a collection of mixing factors (basis vectors) and the other represents target profiles. In some occasions these latent factors can be interpretable. In the “blind source separation” literature a frequently cited example is the “cocktail party problem” where sounds (signals) from multiple sources are mixed up resulting in a combined sound (signal) and the problem to solve is to separate these unique sound (signal) sources. With the assumption that the observed sound is a linear combination of the signals from unique sound sources, our objective is to find a way to compute not only the mixing profiles (basis vectors/latent factors) but also the unique sound sources. In some other domain these latent factors can be completely unobserved and at the same time not interpretable. In general matrix factorization techniques maps the given user-item interaction Y_{uc} into a low dimensional (m) latent factor space defined by the inner product of W_{am} and H_{mc}, where W_{am} represents the item-latitude factor relationship and H_{mc} infers to what extent an user is interested in any item when expressed in terms of that item’s relationship with one or more latent factor(s).

There are a wide variety of literatures (Hoyer, 2002; Wold et al., 1987; Hoyer, 2004; Lee & Seung, 2001; Berry et al., 2006; Su & Khoshgoftaar, 2009; Cichocki & Zdunek, 2007) on matrix factorization. Some of the popular and widely used algorithms in matrix factorization include Spectral Value Decomposition (SVD), Spectral Decomposition Algorithm (SDA) (Srivastava & Buntine, 1995), Non-Negative Matrix Factorization (NMF), Independent Component Analysis (ICA) and Principal Components Analysis (PCA). Although the fundamental idea is same but these machineries consider varying mathematical properties. For example, classical PCA results in a factorization of the matrix into a set of m orthogonal basis vectors. In addition this decomposition technique allows the elements of W_{am} and H_{mc} to be either positive or negative. On the other hand Non-Negative Matrix Factorization finds this decomposition using squared reconstruction error criterion while preserving the non-negativity property over the entire solution space. As we will later demonstrate, some of these properties can be very useful in understanding the underlying data generating process. Researchers typically choose their favorite algorithm based on their understanding about the domain and depending on their goal. However standard matrix factorization techniques must be applied judiciously considering the amount of data or availability of priori knowledge or confidence on the observed data or issue related to over fitting and bias. The research community have proposed several variations (Cichocki & Zdunek, 2007; Koren & Bell, 2011; Koren et al., 2009; Adomavicius & Tuzhilin, 2005) of the standard matrix factorization techniques to take care of the above mentioned issues. Below we provide an overall summary of the state-of-the-art technologies on recommender systems. Further details on each of these bullets can be found in (Koren & Bell, 2011; Koren et al., 2009; Adomavicius & Tuzhilin, 2005).

1. **Content filtering**[Content based information retrieval, Content feature based information filtering]
   (a) **Heuristics based**[Similarity on item’s content based features: e.g., cosine]
   (b) **Model based**[on item’s content based features: e.g.,
2. **Collaborative filtering** \[2 + 1\]

**2. The Competition Problem**

The problem we are trying to solve in this data challenge competition is closely related to remote monitoring and diagnostics in industrial applications. We were provided with three data sets for training. This data was generated from an industrial piece of equipment and no additional information was provided due to proprietary reasons. The equipment has a sensor network to measure several parameters with an onboard condition monitoring system. The measured data goes through a control logic in order to monitor the equipment’s operating regime. At any time instant when some of these parameters meet a specific condition onboard, the control system generates an unique event id/code. It is possible that the control system concurrently triggers multiple events codes if all the necessary conditions are met at the same time instant. To clarify it further: think of any particular case as a set of observations either created by an automated system or manually by an engineer. Each case is described by a set of event codes which characterize the atypical onboard operating condition of the equipment. Some of these cases with specific event code combinations may be operationally significant and could be indicative of “Problem Types”, some of which are assumed to be known to the subject matter experts. As a response to these problems, domain experts may recommend appropriate diagnostic measures (or maintenance actions) depending on the problem types described by a set of the events which have been flagged as a result of atypical operating condition. The goal of this data competition is to build an automated system that can recommend particular maintenance action(s) to mitigate these problem(s).

As mentioned earlier some of these cases are indicative of known “Problem Types” to the subject matter experts. However there could be many examples where a set of cases were not instructive enough to be acted on and hence termed as “Nuisance Cases”. These cases were mostly created by automated systems and were presented to an subject matter expert who determined that the symptom was not sufficient to notify the customer of the identified “Problem Types”. The task of recommending a particular maintenance action, gets relatively easier when these cases have less redundancies in the event combinations. The two major sources of redundancies in this analysis are strong background information of “Nuisance Cases” and overlapping events between “Problem Types”. Given the context, the goal is to accurately recommend confirmed “Problem Types” and avoid making any recommendations for historical “Nuisance Cases”. In this competition the metric used to measure success was in terms of the number of useful outputs. In equation form, the performance of the recommender system \((M)\) was assessed using the following score:

\[
\text{Score}(M) = N_o - N_{mc} - N_n
\]  

where \(N_o\), \(N_{mc}\) and \(N_n\) denotes the total number of outputs, the number of incorrect outputs and the number of nuisance outputs respectively. The number of incorrect outputs is essentially the penalty due to misclassifications i.e. the number of outputs where the true labels and recommender system’s inferred labels do not match. On the other hand the number of nuisance outputs introduces the penalty due to false positives i.e. where the recommender system infers any truly “Nuisance Cases” as one of the “Problem Types”, other than “none”. While evaluating the \(\text{Score}\) (refer Eqn.1) the number of cases with confirmed problems and nuisance test cases are essentially balanced. For the training set, the ground truth is known and hence \(N_{mc}\) and \(N_n\) are known. However for the test set, a total of 174 cases were correctly labeled by the subject matter experts with the known “Problem Types” and the rest as “Nuisance Cases”, although these label information were not available to the participants during the competition. For the test case, the total number of outputs are compared with the known “Problem Types” (174 cases) and a fixed random sample of 174 “Nuisance Cases”. Below we have provided a summary on the data sets provided for training and test purposes.

1. **Train:**
   (a) Case to Problem \((F^{tr}_{cp})\): file contains the different problems associated with each case. (used for training purpose with known “Problem Types”)
   (b) Nuisance Cases \((F^{tr}_{cn})\): file contains a set of cases that were not instructive enough to be acted on. (used for training purpose with unknown “Problem Types”)
   (c) Case to Events and Parameters \((F^{tr}_{cpe})\): file contains the mapping between cases and events and snapshots of the parameters corresponding to each event.

2. **Test:**
served "Event"-"Case" correspondences to the subject matter expert’s understanding about the "Problem Types" given the corresponding cases i.e. "Problem Types"-"Cases" in the event space. This approach also opens up further possibilities of ranking all of the potential choices of maintenance actions according to their likelihood. In the very first step we construct the nuisance case numbers. The file \( F_{\text{ces}} \) consisting of case to events mapping and parameter information has 1316653 rows and 32 columns. The columns represent case number, it’s corresponding event id/code and 30 measured sensor values or parameters, the details of which are unknown. Figure 2 shows the detailed steps to construct \( Y_{\text{ces}} \) and \( Z_{\text{ces}} \). The data preparation recovered 10459 unique train cases and their corresponding 13 unique “Problem Types” and 1242 unique event ids. This means \( Y_{\text{pc}} \) and \( Z_{\text{ec}} \) are of the size of \( 10459 \times 13 \) and \( 1242 \times 10459 \) respectively. The test set \( F_{\text{test}} \) was processes following the same logic as described in figure 2 to construct the “Event”-“Case” scenario \( Z_{\text{ec}} \), except that we considered the same set of unique events ids from training set and ignored the rest of the events to maintain consistency. The size of \( Z_{\text{ec}} \) is \( 1242 \times 9358 \).

### 3.2. Information Retrieval Feature Selection

In the field of information retrieval, the similarity between two entities is often measured by treating each entity as a vector of their occurrences as observed and computing distance between them using some heuristics. In this context, we can think of the columns from \( Z_{\text{ec}} \) matrix as vectors representing the occurrences of the corresponding events over all cases that has been observed. In text mining, documents are often treated as collections of statistically independent words with varying frequencies i.e. documents can be represented as vectors.

### 3.3. Data Preparation

In figure 1 we have shown the steps to accomplish the objective described above. In the very first step we construct the subject matter expert’s understanding about the “Problem Types” given the corresponding cases i.e. “Problem Types”-“Case” correspondences \( Y_{\text{pc}} \) from \( F_{\text{pc}} \) and similarly the observed “Event”-“Case” correspondences to \( Z_{\text{ec}} \) from \( F_{\text{ces}} \). As mentioned earlier, we have ignored the values of the parameters corresponding to each event while constructing \( Z_{\text{ec}} \). \( F_{\text{pc}} \) has 164 rows and two columns, namely case number and corresponding “Problem Types”. \( F_{\text{ces}} \) has 10925 rows with the nuisance case numbers . The file \( F_{\text{ces}} \) consists of case to events mapping and parameter information has 1316653 rows and 32 columns. The columns represent case number, it’s corresponding event id/code and 30 measured sensor values or parameters, the details of which are unknown.

### Figure 1
In this figure we show the basic steps of our approach while accomplishing the goal to predict a good number of unknown “Problem Types” which are truly operational while ignoring the majority of the test cases which may just be nuisance cases.

(a) Case to Problem \( (F_{\text{ces}}^{\text{test}}) \): file contains the different problems associated with each case. (used for testing purpose with unknown “Problem Types”)
as vectors of frequencies with various word observed over the entire corpus. However not all these words are equally informative similar to the event id/cases in our problem. In the text mining paradigm, to successfully retrieve the most relevant document from the entire collection we need to consider building a query using informative words which best describe the document (or similar documents) and at the same time minimize the background noise (avoid redundant words). In text mining community, Inverse Document Frequency (IDF) (Papineni, 2001) is one of the most popular measures of a word’s importance. IDF of a word is measured by taking the logarithmic ratio of counts of total documents to the counts of documents that contains the specific word. Words which appear very frequently across documents are given lower weight as compared to words that appear less frequently among documents. The intuition is that highly frequent words across documents are not a good discriminator. Following the same approach we generate the IDF scores of each event from documents. In the document (or similar documents) and at the same time building a query using informative words which best describe the relevant document from the entire collection we need to consider minimizing the background noise (avoid redundant words). In this context it is worth mentioning that the choice of L − 2 regularization is very instinctive as we intend to restrict large value components and hence reduce chances of over fitting.

The redundancy events are all set to zeros. We will revisit this discussion again in the result section.

### 3.3. Building Model

In this section we will start discussing our model building approach in a more generalized way. However as we proceed further we will simplify the model to fit our problem. This is intentionally done to ensure that the intuition of the mathematical formulation is still consistent with the discussions above. We will start with a matrix decomposition algorithm that can reduce the number of dimensions in the observed signal and here we assume that a set of stationary signals is mixed through a linear mixing matrix. The result of this mixing matrix is the observed signal. The linear model can be expressed as:

\[ Y = WH + E \]  

(2)

In this formulation, \( Y \in R^{p \times c} \) is a matrix of observed data or signals, \( W \in R^{p \times c} \) is the matrix of mixing or basis vectors, \( H \in R^{e \times c} \) represents the hidden source and the \( E \in R^{p \times c} \) matrix represents the noise sources. Here we also assume that there are a total of \( e \) stationary components of \( H \). We will need to solve for \( W \) and \( H \) given the \( Y \) matrix. Our objective will be to minimize the square Euclidean distance \( D(Y \parallel W,H) = \frac{1}{2} \| Y - WH \|^2 \). From the nature of the observed data we know \( Y \) is definitely sparse in nature but \( H \) may not. We don’t make any assumption about the sparsity of \( W \). Instead we introduce \( L - 2 \) regularization terms. In this context it is worth mentioning that the choice of \( L - 2 \) regularization is very instinctive as we intend to restrict large value components and hence reduce chances of over fitting.

The modified cost function looks like,

\[ D(Y \parallel W,H)^{\lambda_1,\lambda_2} = \frac{1}{2} \| Y - WH \|^2 + \lambda_1 \| W \|^2 + \lambda_2 \| H \|^2 \]  

(3)

where \( \lambda_1 \) and \( \lambda_2 \) are user defined regularization parameters. We are essentially minimizing a cost function which is a regularized least-square function. It should be noted that we will also make non-negativity assumptions on \( W \) and \( H \). The above cost function can be made more general by introducing additional constraints like sparsity, offsets, weighting functions etc.

The decomposition procedure starts by assuming a random starting point for \( W \), computing \( H \) and then re-computing \( W \) given the current estimate of \( H \). The updates of \( W \) and \( H \) happen in such a fashion that the cost function is \( D(Y \parallel W,H)^{\lambda_1,\lambda_2} \) minimized. The update equations are based on a least-squares solution to the problem and are derived from the gradients of the cost function (Eqn. 3) with respect to \( W \) and \( H \). When \( \lambda_1 > 0 \) and/or \( \lambda_2 > 0 \), the update scheme takes their effect into account and the cost function gets compensated as a result of the regularized terms.

Although there exists several update schemes for \( W \) and \( H \) (e.g., multiplicative update (Lee & Seung, 2001)), least-squares solutions in particular are extremely favorable to large scale problems. The pseudo code of the update scheme is shown in Fig. 3. The above algorithm is also known as Alternating Least Square (ALS) NMF (Cichocki & Zdunek, 2007; Koren et al., 2009) with the non-negativity constraint on \( W \) and \( H \). For many applications the non-negativity assumption preserves important properties of the observed data and can lead to superior results in some cases. This may also lead to better and more interpretable solutions (Hoyer, 2002; Wold et al., 1987; Hoyer, 2004; Srivastava & Buntine, 1995; Cichocki & Zdunek, 2007; Koren & Bell, 2011).

Matrix factorization techniques feature an easy way to incorporate prior knowledge. For example, suppose we have the initial guess of the either matrix \( W \) or \( H \). The first estimate of \( W \) or \( H \) will result in the optimal (in the least squares sense) result given the initial guess. Subsequent iterations will lead to further refinements in the previous estimates of \( W \) or \( H \). In the current scope of this data challenge, we intend to demonstrate the applicability of the above mentioned algorithms to
map $Y$ into a low dimensional ($e$) event space defined by the inner product of “Problem Types”-events relationship matrix $W$ and events -“Case” relationship $H$. Unlike test data the training data contains known ground truth for all the cases that correspond to “Problem Types” or “Nuisance Cases” and therefore we can compute $Y = Y_{ee}^t$ following the logic explained in (refer Step 11) Fig. 2. If we assume that the blind sources are same as the event combination for each case, then they are essentially known to us, i.e. we can assign $H = Z_{ee}$ (refer Step 10 in Fig. 2). With $Y$ and $H$ known the problem statement boils down to a simple estimation of $W$ and hence we do not update $H$ (Step 2c in Fig. 3) and set $\lambda_2 = 0$, while $W$ was estimated using Step 2a (Fig. 3) with $\lambda_1 \geq 0$.

With $W$ estimated we can reconstruct $\hat{Y}$ and compare it with $Y$ to evaluate the prediction performance using Eqn. 1. In the feature selection stage, the relevant events $e$ from $e$ are chosen based on their IDF scores for which the model $M_e$ maximizes score prediction performance on the training data. However selecting the features using this mechanism may sometimes lead to over fitting.

### 3.4. Results and Discussion

To infer the “Problem Types”, we first preprocess the test data to obtain $Z_{ee}^{tst}$ following the same logic described in Fig. 2 and then estimate $Y_{ee}^{tst} = W H_{ee}^{tst}$, where $H_{ee}^{tst} = Z_{ee}^{tst}$. For this experiment the regularization parameter $\lambda_1$ was tuned to 4. In Table 1 we present the outcome of the recommender for both the training and the test set. The first column of Table 1 represents the identified “Problem Types” and the second and forth column represent the ground truth of the training and test sets respectively. Column 3 & 5 represent the percentage of the accurately predicted “Problem Types” (expressed in %) of all the train and test cases for which the ground truth is known. In the training set there are 13 unique “Problem Types” and a total of 164 cases. However the test set has 14 unique “Problem Types” and a total of 174 cases for which the prediction has to be made. It should be noted that the training data does not contain any examples for P0932 and P6880 types present in the test set and the model is not expected to make any kinds to predictions on these types as they have been anyway eliminated from $F_{ee}^{tr}$ while computing $Z_{ee}^{tst}$ during the pre-processing stage. Beside P2651 type, the prediction accuracy for the rest of the “Problem Types” are considerably worse. The overall accuracies of the prediction on the training and the test sets are 87.5% and 49.3% respectively. There can be many reasons to this poor accuracy on test set, like limited examples of overall “Problem Types” as compared to “Nuisance Cases” in the training set, skewness in the examples of “Problem Types” or even over fitting due to poor selection of tuning parameters. The selection of the tuning parameters can be handled in many different ways as described in (Cichocki & Zdunek, 2007). There exists a huge scope in improving the generalized performance of the ALS NMF based prediction algorithm. It requires some experimentation with different variations of the above mentioned cost function along with an appropriate set of features and correct parameter settings before we obtain the model that best fits this data set.

### 4. Conclusion

This paper has demonstrated the application of a popular collaborative filtering based technique to recommend maintenance actions. In this paper we have discussed the use of standard algorithms like ALS NMF to extract mixture matrix (basis vectors) as a necessary step to predict “Problem Types”. The above mentioned algorithm has demonstrated the ability to predict unknown “Problem Types” for new event sequences. Though ALS NMF based algorithm is better suited for large scale problems, a key weakness of the algorithm, however, is that it assumes that the mixing between $W$ and $H$ is linear. It may be the case that a nonlinear mixing has occurred. Depending on the nature of the nonlinearity, this algorithm may not correctly capture the appropriate basis factors. Another venue to explore is to inspect 2 or 3 top scoring (probable) “Problem Types” for misclassified examples from training set.

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Table 1. In this Table we present the outcome of the recommender for both the training and the test set. The first column of
represents the identified “Problem Types” and the second and forth column represent the ground truth of the training and test
sets respectively. Column 3 & 5 represent the percentage of the accurately predicted “Problem Types” (expressed in %) of all
the train and test cases. Each row represents a “Problem Type” and their corresponding true and predicted values. The overall
statistics is shown in the last row.

| “Problem Types” | Training (true) | Training (predicted %) | Test (true) | Test (Predicted %) |
|-----------------|----------------|------------------------|-------------|-------------------|
| P0159           | 19             | 94.74                  | 15          | 53.33             |
| P0898           | 4              | 50                     | 6           | 50                |
| P1737           | 2              | 50                     | 2           | 0                 |
| P2384           | 53             | 86.79                  | 26          | 69.23             |
| P2651           | 15             | 91.31                  | 13          | 92.31             |
| P3600           | 17             | 88.24                  | 20          | 70                |
| P6559           | 3              | 66.67                  | 1           | 0                 |
| P7547           | 6              | 50                     | 4           | 75                |
| P7695           | 17             | 82.35                  | 37          | 51.35             |
| P7940           | 1              | 100                    | -           | -                 |
| P9766           | 14             | 92.86                  | 12          | 67.66             |
| P9965           | 2              | 50                     | 5           | 40                |
| P9975           | 13             | 92.31                  | 18          | 12.5              |
| P0932           | -              | -                      | 2           | 0                 |
| P6880           | -              | -                      | 15          | 0                 |
| Overall         | 164            | 87.5                   | 174         | 49.43             |

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