From Distributions to Labels:
A Lexical Proficiency Analysis using Learner Corpora

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Abstract
This paper presents work on how we can link word lists derived from learner corpora to target proficiency levels for lexical complexity analysis. The word lists present frequency distributions over different proficiency levels. We present a mapping approach which takes these distributions and maps each word to a single proficiency level. We are also investigating how we can evaluate the mapping from distribution to proficiency level. We show that the distributional profile of words from the essays, informed with the essays’ levels, consistently overlaps with our frequency-based method, in the sense that words holding the same level of proficiency as predicted by our mapping tend to cluster together in a semantic space. In the absence of a gold standard, this information can be useful to see how often a word is associated with the same level in two different models. Also, in this case we have a similarity measure that can show which words are more central to a given level and which words are more peripheral.

1 Introduction
In this work we look at how information from second language learner essay corpora can be used for the evaluation of unseen learner essays. Using a corpus of learner essays which have been graded by well-trained human assessors using the Common European Framework of Reference (CEFR) (Council of Europe, 2001), we extract a list of word distributions over CEFR levels. For the analysis of unseen essays, we want to map each word to a so-called target CEFR level using this word list.

The aim of this project is two-fold: first, we want to create a list of words linked to target proficiency levels. Second, we want to apply this list for lexical complexity analysis of unseen learner essays.

Most vocabulary lists used for second language learner evaluation, such as estimation of vocabulary size, are often derived from native speaker (L1) materials and thus might be ill suited to the needs of second language (L2) learners (François et al., 2016). It is hypothesized that second language learners need to focus on aspects of a language which are not present in native speaker materials (François et al., 2016).

However, such word lists are important for example in essay classification or lexical complexity analysis (Pilán et al., 2016; Volodina et al., 2016a). We thus base our approach on a learner corpus. From this corpus, we extract a list of words with their frequency distributions across proficiency levels. We then link each word to one single proficiency level. In contrast to traditional frequency based proficiency estimations, our approach includes information about learners. We look at “diversity” of a word, i.e. by how many different learners the word has been used at each level. We hypothesize that including diversity scores in the calculation of distribution-to-label mapping yields more reliable and plausible mappings.

The question that remains concerns evaluation. How can we measure the “accuracy” of our mapping in the absence of a gold standard? We address this problem by, on one hand, taking into account expert knowledge from teachers in order to refine the algorithms and, on the other hand, using a second sep-
parate approach to see to what extent both methods overlap.

The method we have chosen for evaluation is a semantic space approach. One of the advantages of the semantic space approach is that it gives us graded results; we can see to what extent words are similar to each other, possibly identifying core vocabulary and peripheral vocabulary at the different proficiency stages.

2 Related work

In the area of Swedish as a second language, several vocabulary lists have been created, such as SVALex (François et al., 2016), SweLL list (Llozhi, 2016), Kelly list (Kilgarriff et al., 2014), the Base Vocabulary Pool (Forsbom, 2006), SveVoc (Mühlenbock and Kokkinakis, 2012) and Swedish Academic Wordlist (Jansson et al., 2012). Of those lists, only SVALex, SweLL list and Kelly list attempted to link vocabulary items to the different proficiency levels according to the Common European Framework of Reference (CEFR) (Council of Europe, 2001), indicating at which level words should be introduced (François et al., 2016).

However, the Kelly list has been compiled from web texts intended for L1 speakers and the vocabulary used for first language (L1) speakers may differ from what beginner second language (L2) speakers need to concentrate on (François et al., 2016). Also, the division into the CEFR levels is based on frequency and the list lacks everyday words useful for learners of Swedish as a second language (François et al., 2016).

SVALex and SweLL list on the other hand have been derived from L2 Swedish material. SVALex has been compiled from the COCTAILL textbook corpus (Volodina et al., 2014) and focuses on receptive vocabulary, while SweLL list has been derived from the SweLL corpus (Volodina et al., 2016b), a corpus of L2 Swedish learner essays, and focuses on productive vocabulary. Neither of these lists link vocabulary items to CEFR levels, but present frequency distributions of lexical items over CEFR levels (Volodina et al., 2014; Volodina et al., 2016b).

In this work we try to use such word lists with frequency distributions over CEFR levels to assign a single CEFR label to each word. This information can be used to analyze texts and visualize the information from a lexical complexity perspective.

3 The learner corpus: SweLL

Our experiments are based on SweLL (Volodina et al., 2016b), a corpus of essays written by Swedish as a second language (L2) learners. The data covers five of the six CEFR levels, namely A1-C1. Table 2 shows the distribution of essays, sentences and tokens per level. Each essay has been manually labeled for CEFR levels by at least two L2 Swedish teachers. The inter-annotator agreement in terms of Krippendorff’s alpha (Krippendorff, 1980) for assigning one of the five CEFR levels was 0.80 which reaches the threshold value specified in (Artstein and Poesio, 2008) for assuring a good annotation quality. Furthermore, the texts have been automatically annotated across different linguistic dimensions including lemmatization, part-of-speech (POS) tagging and dependency parsing using the Sparv (previously known as ‘Korp’) pipeline (Borin et al., 2012). The essays encompass a variety of topics and genres and they are accompanied by meta-information on learners’ mother tongue(s), age, gender, education level, the exam setting.

| Level | Nr essays | Nr tokens |
|-------|-----------|-----------|
| A1    | 16        | 2084      |
| A2    | 83        | 18349     |
| B1    | 76        | 30131     |
| B2    | 74        | 32691     |
| C1    | 90        | 60832     |
| Total | 339       | 144 087   |

Table 1: Number of items per CEFR level

4 Extracting the data

We extract a list of words and their frequency distributions over CEFR levels from the SweLL corpus. In contrast to the earlier SweLL list (Llozhi, 2016), we calculate relative frequencies for each level and extract further information such as learner counts and topics over levels.

Table 2 exemplifies the resulting data. In the first column, we have the lemma of a word, in the second column the corresponding part of speech, fol-
Table 2: Extracted data: Example

| lemma | pos | A1  | A2  | B1  | ... | LI A1 | LI A2 | LI B1 | ... | T A1 | T A2 |
|-------|-----|-----|-----|-----|-----|------|------|------|-----|------|------|
| göra  | VB  | 0.12| 0.23| 0.61| ... | x2, b1, a3, c7 | x1, y1, z9 | ... | everyday life |

... heta VB 0.10 0.22 0.46 ... x1, b3, y6, z3 k2, l1, m1 n2, p1 ... personal info ...

5 From distributions to labels

In order to link lexical items to CEFR levels, we have to define how we map from a frequency distribution over CEFR levels to a single level. The following sections describe the algorithm, the problem of why we can’t directly map frequency distributions to labels, and word diversity normalization, which solves this problem.

5.1 Algorithm

In contrast to receptive vocabulary lists, the concept of ‘target level’, i.e. at which level a word should be understandable, is not applicable to word lists derived from productive vocabulary.

Instead, we look at the significant onset of use, i.e. at which level a word is used significantly more often than at the preceding level.

In order to calculate the significant onset of use, for each word we calculate the score $D_i$ at level $i$ as the difference in frequencies between the current level $i$ and the previous level $i-1$ as shown in equation 1. If $i = A1$, $f_{i-1} = 0$.

$$D_i = |f_i - f_{i-1}|$$  \hspace{1cm} (1)

If $D_i$ is higher than a certain threshold value, we take the level $i$ as label for the word. Based on initial empirical investigations with L2 teachers that rate the overlap between teacher- and system-assigned levels, we have found that a threshold value of 0.4 works well; lower threshold values exclude relevant words from a certain level while higher threshold values include words which are deemed to be of a different level.

5.2 The problem

If we look at the data, we can see that mapping distributions to labels is not straightforward, e.g. figures 1 and 2 show the distributions of the words heta (verb) ‘to be called’ and göra (verb) ‘to do’. Using the significant onset of use algorithm, we would predict B1 as label for these words.

![Figure 1: Frequency distribution of the word heta ‘to be called’](image1)

![Figure 2: Frequency distribution of the word göra ‘to do’](image2)

However, those words will most probably be used earlier by learners, since CEFR, inter alia, defines CEFR proficiency levels through topics. For example, the CEFR document states that one should be able to “introduce him/herself and others and [...] ask and answer questions about personal details such as where they live, people he/she knows and things he/she has” (Council of Europe, 2001, page 24).
The verbs göra and heta are encountered very often at the beginner level as beginners learn to introduce themselves (e.g. Jag heter Peter. ‘My name is Peter.’) and talk about things they do.

Thus, common sense dictates that we cannot simply use frequency distributions as indicators of when learners should be assumed to be able to start using certain words productively.

5.3 Word diversity
In contrast to directly mapping frequency distributions to labels, we have found that normalizing the frequencies using word diversity improved results significantly. We calculate word diversity for each word by looking at how often the word was used at each level and how many different learners used the word at each level. Word diversity of a word \( w \) at level \( L \) is calculated by dividing the number of occurrences of the word at level \( L \) by the number of distinct learners \( d \) that used the word at that level as shown in equation 2. The intuition is that if a word is used often at a certain level, but only by one learner, it is less representative of this level than if it is used by many different learners.

\[
diversity(w, L) = \frac{\text{count}(w, L)}{\text{count}(d, w, L)} \tag{2}
\]

After normalizing the original frequency distribution to fit into the interval 0-1, we average the word diversity distribution and the normalized frequency distribution to arrive at a new distribution. Figure 3 shows the new distribution for heta.

![Figure 3: New distribution of the word heta ‘to be called’](image)

We can see that including word diversity shifts the original frequency distribution towards the left, with a peak at A1. Incidentally, the automatically predicted level for this word is also A1; however, it should be noted that the calculation of the significant onset of use differs from simply taking the peak. For example, figure 4 shows the recalculated distribution for the relatively common verb göra ‘to do’. We can see maxima at A2 and B2, but the algorithm predicts the more plausible A1.

![Figure 4: New distribution of the word göra ‘to do’](image)

6 Distributional semantics
We used the gensim implementation of Word2Vec (Mikolov and Dean, 2013) to create a vector space model of our corpus of essays. Since we don’t have a gold standard to validate our results, we wanted to see to what extent we might reproduce the same essay level labeling through a different method. We have 339 essays, each one labeled with a CEFR grade as assigned by a teacher. Given this data, we built two different kinds of semantic spaces: a simple context-based space taking into account a number of words at the left and right of the given lemma; and an “indexed” approach which, for each word in an essay, takes into account both its context and the proficiency level of the whole essay. In other terms, the proficiency level of an essay is treated as contextual information to build a word’s distributional vector, in the same way as other words. We also tried a stricter approach where we constrained the system to take into consideration only the proficiency level to build the distributional vector of a lemma, under the assumption that words sharing the same proficiency-related distributional profile would tendentially cluster together in a semantic space, without need for further information.

It is important to understand what kind of spaces these approaches create. If we don’t take proficiency levels directly into account, we generate a traditional semantic space where words that have similar contexts cluster together. The problem in creating consistent proficiency-related vocabularies with this approach is clear: if a C1 word happens to be a synonym of an A1 word (and thus used in similar contexts) it will be more similar to such A1 word than to other C1 words.

If we take into account both context and proficiency levels, proficiency level labels become them-
selves “points” in the multidimensional semantic space: thus, words that occur in the same level will tend to be near, but also a word will be nearer to the proficiency label it shares most context with. The advantage of this method is that we can directly compute the similarity between a lemma and a proficiency level; the disadvantage is that contextual information could actually work as noise. For example, if a complex word as *angelägenheter* ‘concerns’ (noun) co-occurs with a simple word as *tisdag* ‘Tuesday’, and *tisdag* mainly happens at level A1, then *angelägenheter* and the point ‘A1’ will become closer.

If, finally, we only take into account the proficiency level, words that occur in the same level will be similar in the semantic space. In this case we cannot meaningfully compute a word-level similarity but the risks of contextual noise are reduced. It can be interesting to note that since we are using a continuous semantic space we can try to predict the proficiency level (in a direct or indirect way) of full documents by averaging the individual vectors of their words.

We can use one of these models to compute the direct cosine similarity between a word and a level and that we could use to check whether the most similar words to a given word. For example, given the word *eftersom* ‘because’, we select the label holding the nearest cosine similarity with it, for example “A2”; if *eftersom* is mapped to the level A2 according to our mapping algorithm, we have an agreement among our models. We can then count how many “nearest labels” coincided with the frequency-based prediction and determine to what extent the two approaches are consistent in modeling the data.

The second test consists in simply retrieving, for every word, its *n*-nearest neighbours in the semantic space. We can then determine whether these neighbours belong to the same proficiency level of the given word in the frequency list. For example, we can retrieve the nearest neighbours of the word *tisdag* ‘Tuesday’ and find them to be *lördag* ‘Saturday’ and *trött* ‘tired’. If these two words are of the same proficiency level as *tisdag* in our lists, we can suppose a certain consistency between the two approaches.

Table 3 shows the results for the different tests and different models. We tested two indexed models, with window size 1 and 60 respectively, and a non-indexed model with window size 10. The numbers indicate how many items were assigned the same proficiency levels in both the semantic space model and the frequency-based mapping, with the upper limit being 100. We are indicating counts, but as the upper limit is 100, the numbers can also be understood as percentages. For the word-word similarity test, we look at the first, second and third most similar words according to the cosine similarity and check whether their proficiency label is the same as the one assigned by the frequency-based mapping. The figures in parentheses indicate the number of close mismatches (off-by-one errors).

Apparently, an “indexed” semantic space with a large window shows the highest agreement with our model. Considering that we are predicting labels
over five proficiency levels, accuracies of 51% and 67% are encouraging numbers. What is maybe even more interesting is the number of close mismatches. These cases are interesting because they could show that the models are setting different boundaries, but tendentially agree on the general progression of the vocabulary. If the number of close mismatches is high, it means that we have many cases where A1 words (in our frequency list) are “labeled” as, or cluster with, A2 words in the semantic space: it is easy to see that similar cases are qualitatively very different from cases where an A1 word clusters with C1 vocabulary. The large presence of similar cases in our results brings us the next reason that induced us to use semantic spaces: they can give nuanced results. If we use a distributional space to label a lemma, we’ll have not only the most probable level of such lemma, but also its distance to the next and previous level. For example, both our frequency list and our best performing semantic space label resa ‘to travel’ as an A2 word. From the semantic space, we can also see that it is much closer to B1 than to A1 – we can suppose that it is a rather “advanced” word that tends to lie between A2 and B1. In the same way, fredag ‘Friday’, labeled as A2 by the frequency lists, clusters in our space both with A2 and (less closely) A1 lemmas, showing that it is likely to be a term on the “easy” spectrum of the A2 vocabulary.

8 Lexical complexity analysis

In order to analyze an unseen learner essay, we annotate the essay using the Sparv pipeline (Borin et al., 2012). This step results in a lemmatized and part-of-speech tagged text. Each lemma is then looked up in the previously calculated word list and marked as being of the level indicated in the word list.

We can then simply visualize this information using a graphical user interface¹ as shown in figure 5. After entering a text in the text box, it is possible to highlight words of certain CEFR levels. This kind of visualization can give a good impression of the distribution of word levels in a text.

![Figure 5: Text evaluation: Visualization](https://spraakbanken.gu.se/larkalabb/texteval)

We can also use the word list to predict the overall proficiency level of the essay. Rather than being used on its own, it is incorporated into larger systems. Recent research has shown that substituting traditional frequency based lists by distributionally mapped word lists in machine learning based automatic essay grading systems results in significantly better predictions (Pilán et al., 2016).

9 Conclusion

In this paper we have shown how lists of frequency distributions of lexical items over CEFR levels can be used for lexical complexity analysis by linking each word to a single CEFR label. We have found that augmenting frequency based lists with learner counts yields more plausible mappings than taking into account only the frequency information. Using a semantic space approach we have shown that our results are consistent across different models. Finally, we have shown how this information can be visualized and used for essay grade prediction.

¹https://spraakbanken.gu.se/larkalabb/texteval
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