Ultrafast tilting of the dispersion of a photonic crystal and adiabatic spectral compression of light pulses

Daryl M. Beggs,1,2 Thomas F. Krauss,2 L. Kuipers,1,* and Tobias Kampfrath1,3

1FOM Institute AMOLF, Science Park 104, 1098 XG Amsterdam, The Netherlands
2School of Physics and Astronomy, University of St. Andrews, St. Andrews, Fife, KY16 9SS, UK
3Fritz Haber Institute of the Max Planck Society, Faradayweg 4-6, 14195 Berlin, Germany

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We demonstrate, by theory and experiment, the ultrafast tilting of the dispersion curve of a photonic-crystal waveguide following the absorption of a femtosecond pump pulse. By shaping the pump-beam cross section with a nanometric shadow mask, different waveguide eigenmodes acquire different spatial overlap with the perturbing pump, leading to a local flattening of the dispersion by up to 11%. We find that such partial mode perturbation can be used to adiabatically compress the spectrum of a light pulse traveling through the waveguide.

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Physical systems can often be described by their eigenmodes, that is, states of light or matter oscillating with a well-defined frequency. For instance, the quantum-mechanical eigenstates of an electron spin are spin-up and spin-down [1], while the optical eigenmodes of a photonic crystal are Bloch waves characterized by their wavevector \( k \) and angular frequency \( \omega_k \) [2]. Controlling the eigenfrequencies allows for the reversible manipulation of light and matter, provided the dynamics evolve adiabatically, without exchange of energy between the eigenmodes. As an example, adiabatically changing the frequency spacing of spin states is nowadays routinely employed to cool solids [1] or to control the precession of a single spin [3]. The state-dependent change in eigenfrequencies is realized by an external magnetic or electric field which couples differently to spin-up and spin-down states.

Usually, however, optical eigenmodes (such as those of photonic crystals or microresonators) are perturbed by a homogeneous and isotropic stimulus, leading to one and the same shift of all the eigenfrequencies [4–9]. A much higher level of control could be achieved if one allows for a spatially varying perturbation that has different overlap with the light field of different modes. Such a process would result in a modified frequency spacing and density of states [10], which is particularly interesting for a photonic crystal with its continuum of modes \( k \). Figure 1(a) shows that a \( k \)-dependent mode-shift \( \Delta \omega_k \) would lead to a local tilting of the photonic dispersion \( \omega_k \). A light pulse being a superposition of these wavefunctions could then be spectrally compressed and temporally stretched, provided the dynamics were adiabatic. Moreover, as first proposed by Yanik and Fan [11], such pulse could be also slowed down beyond the classical delay-bandwidth limitation.

In this Letter, we demonstrate that perturbing selected regions of a photonic-crystal waveguide (PCW) by means of a spatially shaped femtosecond laser pulse can locally flatten or steepen the dispersion curve. This novel procedure is akin to altering the shape of the “potential” confining the wavefunctions, thereby realizing a new dispersion relationship and density of states [2]. Such partial mode perturbation (PMP) can be used to compress or expand the spectrum of a picosecond light pulse traveling through the waveguide. As this operation proceeds adiabatically, it is reversible and features high conversion efficiency.

Our nanophotonic approach is schematically shown in Fig. 1(b). Whilst a light pulse travels through a PCW, a pump pulse incident from above generates an electron-hole plasma in the Si parts of the structure, thereby reducing the refractive index. The index change does not occur in the waveguide center as a shadow mask keeps pump light away from that region. Since PCW eigenmodes have a strongly \( k \)-dependent lateral extent [Fig. 2(a)], each mode \( k \) has a different spatial overlap with

![Figure 1](https://example.com/figure1.png)

FIG. 1: (a) Schematic of adiabatic light control. An input light pulse excites eigenmodes of a photonic crystal, whose dispersion \( \omega_k \) is then blueshifted and flattened by an external perturbation. When no light is scattered between eigenmodes, the pulse undergoes an adiabatic spectral compression. (b) Experimental realization. Whilst a probe pulse travels through a Si-based photonic-crystal waveguide, a pump pulse generates free charge carriers in the illuminated Si regions. The shadow mask causes a \( k \)-dependent spatial overlap between waveguide mode and pump pattern.
the pumped Si volume, resulting in a pronounced variation of the mode-shift $\Delta \omega_k$ with respect to $k$. Note that the dynamics of the probe pulse inside the waveguide will proceed adiabatically because the pump pulse respects all spatial symmetries of the PCW [3, 11]. Breaking these symmetries would result in energy transfer between different modes [12] as has been shown in a complementary experiment [13].

**Theory.** We first explore our approach theoretically. To this end, we consider the frequency shift $\Delta \omega_k$ of mode $k$ that results when the pump pulse alters the refractive-index landscape of the photonic crystal by an amount $f(r) \Delta n$. Here, $0 \leq f(r) \leq 1$ reflects the normalized spatial distribution of the absorbed pump energy, which induces a change $\Delta n$ in the real part of the refractive index at positions $r$ where $f(r) = 1$. Perturbation theory [2] then predicts a relative eigenfrequency shift

$$\frac{\Delta \omega_k}{\omega_k} = - \frac{\Delta n}{n} O_k$$

which is directly proportional to the spatial overlap

$$O_k = \int d^3r \, f(r) u_k(r)$$

between the profiles of perturbation and eigenmode. In these relations, $n = 3.48$ denotes the refractive index of the unpumped Si, and $u_k(r)$ is the energy density of mode $k$ normalized according to $\int d^3r \, u_k(r) = 1$.

In order to tilt the dispersion, $O_k$ needs to be $k$-dependent. More precisely, we have to realize a relative change $\Delta v_k/v_k$ in the local slope $v_k = \partial \omega_k/\partial k$ of the dispersion curve that is much larger than the perturbation $\Delta n/n$. Note that $\Delta v_k/v_k$ also quantifies the relative velocity change and relative spectral compression [Fig. 1(a)] of a light pulse encountering the dispersion change on-the-fly. In this respect, PCWs offer two unique benefits. First, the lateral mode extent depends strongly on $k$ as seen in Fig. 2(a) [14, 15]. Second, using the slow-light modes with low group velocity $v_k$ means that $\Delta v_k/v_k$ can be enhanced for a given $\Delta n/n$ [3].

We calculated the eigenmodes [16] of a PCW [Fig. 1(b)], which can be pictured as a missing row of holes in a Si membrane (thickness 220 nm), perforated with a hexagonal pattern of holes (lattice period $a = 390$ nm, hole diameter 220 nm). The PCW (length $L = 180a = 70.2 \mu m$) has a 600-nm thick SiO$_2$ cladding on top of which a Au stripe (675 nm wide, 20 nm thick) serves as a shadow mask. The overlap and, thus, the interaction between mask and the evanescent tail of light inside the waveguide are negligible. Figure 2(a) displays the unit cell of the PCW and the profile $u_k(r)$ of the electromagnetic energy density for several modes $k$. The respective values of $k$ can be inferred from the points labeled (i) to (xi) in the dispersion curve $\omega_k$ of Fig. 2(b). With increasing $k$, the slope of $\omega_k$ and, thus, the group velocity decrease continuously, ending up in a flat dispersion being characteristic of slow light ($v_k < c/50$ at $ka/2\pi > 0.45$) [17]. As seen in Fig. 2(a), the transition from fast to slow light is accompanied by drastic changes in the spatial mode profile [14, 15]. Whereas the light field of modes (i) and (ii) lies nearly entirely under the shadow mask, it spreads out into the surrounding lattice of holes for modes (iii) to (v) and then starts to contract again for modes (vi) to (xi).

The $k$-dependent lateral mode spread should be also reflected by the overlap $O_k$ of mode profile and pump pattern, as long as the mask’s shadow on the Si surface is not washed out by diffraction of the pump beam. Finite-difference time-domain simulations [18] of the pump-pulse propagation indeed verify that $f(r)$ roughly follows the shape of the mask’s geometric shadow [inset of Fig. 2(c)]. The resulting overlap [Eq. (2)] of $f$ with the waveguide modes is shown in Fig. 2(c) and exhibits the expected behavior: a steep rise for low wavevectors followed by a flatter decay at higher $k$. Thus, any pulse populating these modes will be spectrally compressed or expanded upon the dynamic action of the perturbation. For comparison, the dashed line shows the frequency shift for the case of a homogeneous perturbation profile ($f = 1$ throughout the Si). The $k$ dependence of $O_k$ nearly vanishes because the total amount of mode energy inside the Si material is almost independent of $k$.

**Experiment.** In order to put our PMP scheme to test, we fabricated a masked PCW with the same geometrical parameters used in the calculations by means of electron-beam lithography and reactive ion etching. After filling with SiO$_2$, a Au shadow mask is placed on top of the SiO$_2$ cladding by metal evaporation and lift-off. In order to excite the PCW, pump pulses (center wavelength 810 nm, duration 100 fs full width at half maximum of the intensity, pulse energy 2 nJ, repetition rate 80 MHz) from a Ti:sapphire laser pass a slit and cylindrical lenses in a two-dimensional data set $E_\omega(\omega, \tau)$. By varying the delay between pump and probe pulse, we obtain a two-dimensional data set $E_\omega(\omega, \tau)$. Figure 2(d) shows the real part of the measured $E_\omega(\omega, \tau)$ at 40 ps before PCW pumping ($\tau = -40$ ps, red line) and at 1 ps after ($\tau = 1$ ps, blue line). In both cases, two regimes with slow and fast oscillations are observed. Assuming single-mode propagation, the phase acquired by the probe pulse after propagation through the PCW equals $k(\omega)L$. Thus, $Re E_\omega = |E_\omega| \cos(kL)$ versus $\omega$ oscillates more rapidly for slower light as the inverse group velocity $\partial k/\partial \omega$ is larger. Therefore, the fast and slow oscillations in Fig. 2(d) are signatures of slow and fast light, respectively. Solving for the phase of $E_\omega$ allows...
us to extract the wavevector \( k \) as a function of \( \omega \) (apart from an unknown offset since only phase differences can be measured). The so-obtained waveguide dispersion \( \omega_k \) is shown in Fig. 2(c) before and after Si pumping. One clearly recognizes the regions of fast and slow light, and the shape of both curves is in very good agreement with that of the one calculated [Fig. 2(b)].

A superficial glance at Fig. 2(e) might lead to the notion that the dispersion directly after PCW pumping (\( \tau = 1 \) ps) is just a blueshifted version of the dispersion of the unpumped waveguide. However, a magnified view [inset of Fig. 2(e)] reveals departures from such rigid-shift-type behavior. This observation becomes even more apparent when we subtract one of the dispersion curves from the other. Figure 2(f) presents the resulting pump-induced mode-shift \( \Delta \omega_k \) at various delays after PCW pumping. Shortly after excitation (\( \tau = 1 \) ps), the mode-shift varies strongly with the wavevector, from \( \Delta \omega_k /2\pi = 0.060 \) THz (at \( ka/2\pi = 0.33 \)) to over 0.120 THz (0.38), before dropping back to 0.095 THz (0.45). This curve agrees excellently with the theoretical prediction [solid line in Fig. 2(c), gray dashed line in Fig. 2(f)]. Comparison of the calculated overlap \( O_k \) and the measured mode-shift \( \Delta \omega_k \) with Eq. (1) allows us to estimate the pump-induced change in the Si refractive index to \( \Delta n/n \approx -1.5 \times 10^{-3} \). Interestingly, at \( ka/2\pi = 0.37 \) [arrows in Figs. 2(e) and 2(f)], the measured \( \Delta \omega_k \) and, thus, \( O_k \) have a quite steep slope whereas the slope of \( \omega_k \) is rather flat, resulting in a measured ratio \( \Delta \omega_k /\omega_k \) of as much as 12%. This value is more than 80 times larger than the perturbation \( \Delta n/n \), showing that our nanophotonic approach [Fig. 1(b)] indeed causes a strongly \( k \)-dependent frequency shift of the photonic-crystal eigenmodes.

At later times after pump excitation, charge-carrier diffusion and recombination in Si are expected to modify the refractive-index distribution \( f(r) \Delta n \). Indeed, with increasing delay \( \tau \), the measured \( \Delta \omega_k \) [Fig. 2(f)] undergoes an overall decrease and returns into a flat line (\( \tau \geq 250 \) ps). This final, virtually \( k \)-independent mode-shift agrees well with the calculated \( \Delta \omega_k \) for a homogeneous excitation pattern [dashed line in Fig. 2(c)]. Thus, after about 250 ps, the pump-induced charge carriers have diffused into the Si underneath the 675 nm wide shadow mask, resulting in a homogenised carrier density. These numbers allow us to estimate a mean diffusion constant of \( \sim 10 \text{ cm}^2 \text{s}^{-1} \), which is in good agreement with previous measurements \([21]\). Whereas the observed flattening of the dispersion change arises from carrier diffusion, the temporal decrease of the \( k \)-averaged \( \Delta \omega_k \) on a time scale of about 500 ps is a consequence of carrier recombination, predominantly taking place at the surface of the PCW \([10]\).

**Spectral compression.** We finally illustrate how the ultrafast modifications of the PCW dispersion can be used to spectrally compress a light pulse. For this purpose, we consider a Fourier-limited Gaussian pulse with a duration of 1.9 ps and a center frequency of 194.2 THz as PCW

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**FIG. 2: Theoretical [(a)-(c)] and experimental [(d)-(f)] results for the waveguide dispersion changes.** (a) Bottom panel: shape of unit cell of photonic-crystal waveguide together with shadow mask. Panels (i) to (xi): profiles of electromagnetic energy density \( u_k(r) \) of selected waveguide eigenmodes with \( k \) indicated in (b). Note the logarithmic color scale. (b) Dispersion \( \omega_k \) of the waveguide eigenfrequencies. (c) Solid line: calculated overlap (see inset) and the pump pattern \( f(r) \) given by the shadow mask (inset). Dashed line: \( O_k \) for a spatially uniform change in the Si refractive index. (d) Measured real part of the Fourier-transformed output pulse \( E_\omega(\omega, \tau) \) versus \( \omega \) at 40 ps before (red) and 1 ps after (blue) waveguide pumping. (e) Dispersion curves of unpumped and pumped waveguides as extracted from (d). (f) Dispersion shift \( \Delta \omega_k \) at several delay times obtained by subtraction of the measured \( \omega_k \) [see (e)]. Dashed gray line: theoretical curve of Fig. 2(c), repeated for comparison. Bar: error estimated from signal variations at delays \( \tau < -15 \) ps.
When the pump-induced shift $\Delta \omega$ leads to additional light absorption, the output pulse is smaller in the excited case because unexcited or excited waveguide, respectively. The energy of the mode-shift occurring long before, after, or while the probe is inside the waveguide. Spectra are normalized to same height and shifted to have center frequency $\omega = 0$. Input [arrows in Figs. 2(e) and 2(f)] for the following two reasons. First, the spectrum coincides with a part of the dispersion that undergoes a significant pump-induced flattening $\Delta \nu_k/\nu_k$ (see above). Second, this pulse allows one to confine 96% of its energy within the length of the waveguide as its duration is significantly shorter than its transit time of 5.6 ps.

We are able to determine the PCW response to the fictitious 1.9-ps input pulse from the two-dimensional data set $E_o(\omega, \tau)$ [Fig. 2(d)] that was measured using the much more broadband 180-fs probe pulse. This approach merely presumes that the waveguide response to the weak probe pulse is linear, which we have verified experimentally. The extracted output spectrum is shown in Fig. 3(a) as a function of the delay between pump and probe pulse. At delays $\tau < -5$ ps and $\tau > 5$ ps, no dynamics occur as the probe pulse encounters a fully unexicted or excited waveguide, respectively. The energy of the output pulse is smaller in the excited case because free charge carriers lead to additional light absorption. At $\tau = 0$, the probe pulse is fully contained in the PCW when the pump-induced shift $\Delta \omega_k$ of the dispersion curve occurs. As the light populating these modes is frequency-shifted as well [Fig. 1(a)], we find a clear blueshift of the PCW output around $\tau = 0$ [Fig. 3(a)]. The center frequency increases by 0.12 THz, in good agreement with the magnitude of the measured $\Delta \omega_k$ [Fig. 2(f)].

In conclusion, we have demonstrated that partial mode perturbation can be used for all-optical adiabatic pulse-bandwidth compression. This process is significant because it overcomes the fundamental bandwidth-delay constraint in optics. Ultimately, such a process can generate arbitrarily small group velocities for any light pulse with a given bandwidth, without the need for intrinsic material resonances. The unavoidable signal loss due to free-carrier absorption could be prevented by using tuning mechanisms like the instantaneous optical Kerr effect. Besides the dynamical slow-down of light, spectral compression could also find application as a magnifying time lens: the uniform shrinking of the frequency axis by a factor $1 + \Delta \nu_k/\nu_k$ yields an expansion of the pulse by the inverse factor in the time domain. The magnitude of the spectral compression could be enhanced further by optimizing the profiles of the perturbing pump or by modifying the photonic crystal itself. One could repeat the spectral compression in cascaded photonic crystals: the smaller the bandwidth of the pulse becomes, the smaller the slope of the dispersion of the next waveguide-stage can be chosen, leading to a larger relative compression $\Delta \nu_k/\nu_k$.

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