Hyperons in thermal QCD
A lattice view
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I. INTRODUCTION

How the light hadrons behave under the extreme conditions of nonzero temperature and/or density is a question of fundamental importance, linked to confinement and chiral symmetry. Moreover, quantitative insight is highly relevant for ongoing heavy-ion collision experiments, exploring the QCD phase diagram, as heavy-ion phenomenology relies on understanding the behavior of hadrons under the conditions created in those collisions.

A widely used description of the hadronic phase at nonzero temperature and vanishing or low baryon density is given by the hadron resonance gas (HRG) [1–3], in which all states, including resonances, contribute to thermodynamic quantities, such as pressure, entropy and susceptibilities. In its simplest form, the hadrons are treated as noninteracting particles, characterized by their vacuum mass and quantum numbers. This setup gives a reasonable description of both heavy-ion phenomenology [4,5] and lattice QCD data [6,7]. A closer look, however, reveals intriguing discrepancies [8,9]. This is not unexpected and there are a number of HRG modifications which aim to go beyond the ideal HRG, e.g., by including attractive and/or repulsive interactions [10,11], hard-core interactions [12] or additional states, predicted by e.g., the quark model but not yet observed in nature [8,9,13].

Most commonly used implementations of the HRG, however, use a formulation in which the resonances have the same mass throughout the hadronic part of the QCD phase diagram, i.e., equal to their value in vacuum. This is somewhat surprising, since the in-medium modification of masses, or of more general spectral features, is a longstanding topic of interest in the theory and phenomenology of strongly interacting matter and often used as one of the indications of the presence of a medium [14,15]. For light hadrons, chiral symmetry is expected to play an important role and in-medium effects are often captured by a medium-dependent chiral condensate. While this is widely accepted, it is typically not implemented in the HRG or its extensions. An exception is Ref. [16], in which the interplay between the freeze-out temperature and chiral-condensate dependent in-medium masses has been discussed.

There is therefore a need to unambiguously establish if and how the masses of the light hadrons in the hadronic phase depend on the temperature, at zero and low baryon density. This is a nonperturbative question in QCD, which can be addressed using either a first-principle lattice QCD computation or via effective models, suitably benchmarked against lattice QCD results. While mesons at finite temperature have indeed been fairly well studied on the lattice in various contexts (see e.g., Ref. [17] for a list of references), for baryons this is not the case. In fact, there are only a few lattice studies of baryonic thermal screening [18,19] and...
temporal [17,20,21] masses. Here we extend our work on baryons [17,21], using lattice QCD simulations on the FASTSUM anisotropic \( N_f = 2 + 1 \) ensembles [22,23], to include hyperons, i.e., all octet and decuplet baryons. We are particularly interested in the role of chiral symmetry and the emergence of parity doubling: in the presence of unbroken chiral symmetry, positive- and negative-parity baryonic channels are degenerate. When chiral symmetry is (spontaneously) broken, this is no longer the case and indeed, in vacuum the positive-parity ground state is typically lighter than the negative-parity one. Since chiral symmetry is restored around the deconfinement transition, one expects a degeneracy to emerge, based purely on symmetry considerations. Here we investigate how this degeneracy emerges, which is a nonperturbative dynamical question, not answerable using symmetry considerations alone, and how it affects the HRG description.

The paper is organized as follows. In the following section we summarize the details of the lattice QCD simulations [22,23]. Section III contains the results on temperature effects in the hadronic phase at vanishing baryon density, including a parametrization of the temperature-dependent masses for the negative-parity ground states. These parametrizations are subsequently used in Sec. IV to define an in-medium hadron resonance gas, and we give an application to baryonic fluctuations and contributions to the pressure. Section V contains the results in the deconfined phase, including an analysis of the strangeness dependence of the transition from the low- to the high-temperature phase. A summary is given in Sec. VI. The \( N, \Delta \) and \( \Omega \) channels were already discussed in Ref. [17]; preliminary results in the \( \Lambda, \Sigma, \Sigma^\ast, \Xi \) and \( \Xi^\ast \) channels have been presented in Ref. [24].

II. LATTICE QCD DETAILS

In order to investigate QCD at nonzero temperature nonperturbatively, the FASTSUM collaboration uses lattice QCD simulations on highly anisotropic lattices, \( a_\tau / a_s \ll 1 \). We employ a fixed-scale approach in which the temperature is varied by changing the number of time slices \( N_\tau \), via the standard relation, \( T = 1/(a_\tau N_\tau) \). The choice of fixed-scale anisotropic lattices is specifically motivated for spectral studies of QCD at nonzero temperature, as it increases the number of time slices available and does not require a zero-temperature tuning of parameters for each temperature value. Our lattice discretization follows the Hadron Spectrum Collaboration [25] and uses a Symanzik-improved anisotropic gauge action with tree-level field coefficients and a mean-field–improved Wilson-clover fermion action with stout-smeared links [26]. Full details can be found in Refs. [22,23].

We have available several ensembles, four below and four above the deconfinement transition, see Table I. These ensembles make up our Generation 2 ensembles and have been used in studies of transport [23,27], bottomonium [22], open and hidden charm [28], and baryons [17,21], which are further studied in this paper. Tuning of the lattice parameters and also the “zero-temperature” ensemble \( (N_\tau = 128) \) were kindly provided by the HadSpec collaboration [25]. The crossover temperature, denoted with \( T_c \), is determined via the inflection point of the renormalized Polyakov loop and is found to be \( T_c = 185(4) \) MeV. This is higher than in nature, due to the light quarks not having their physical masses \( (m_q = 384(4) \) MeV). The strange quark mass has its physical value [22,23]. We note here that in the case of a crossover the transition temperature determined via other observables, e.g., linked to chiral properties, can be different, see e.g., Ref. [6]. Here we use \( T_c \) to denote the transition temperature determined via the Polyakov loop, as discussed above, and take care to distinguish it from estimates coming from other observables.

For the baryonic correlators, we apply Gaussian smearing [29] at both the source and the sink in the spatial directions, in order to increase the overlap with the ground state. The smearing parameters are chosen to maximize the length of the plateau for the effective mass of the ground state. These smearing parameters are then used at all temperatures, see Refs. [17,21].

III. IN-MEDIUM EFFECTS IN THE HADRONIC PHASE

We computed all octet (spin 1/2) and decuplet (spin 3/2) baryon correlators, for both positive and negative parity. In fact, in each channel the parity partners are encoded in the same Euclidean correlator: if \( G_\pm(x) \) denotes the correlator projected to positive (negative) parity, i.e.,

\[
G_\pm(x) = \langle \text{tr} P_\pm O(x) \bar{O}(0) \rangle, \quad P_\pm = \frac{1}{2}(1 \pm \gamma_4),
\]

with \( O(x) \) the baryon annihilation operator, then

\[
G_\pm(1/T - \tau, \mathbf{p}) = -G_\mp(\tau, \mathbf{p}),
\]
i.e., the parity partner propagates from the opposite side of the Euclidean lattice; see Ref. [17] for a detailed derivation.

In the confined phase, we find that the correlators can be described by combinations of exponentials, allowing us to determine the ground state masses $m_{\pm}$ as a function of the temperature. Examples of correlators and a description of fitting methods can be found in Ref. [17]; we follow the same approach here. Our results for the ground state masses, $m_{\pm}(T)$, in both parity channels at four temperatures in the confined phase are given in Table II, together with the “zero-temperature” results from the Particle Data Group [30]. As mentioned above, the results for the $N$, $\Delta$ and $\Omega$ baryons were previously presented in Ref. [17].

A few things can be noted. We start at the lowest temperature. Since the light quarks are somewhat heavy, the $S = 0$ states at the lowest temperature are also heavier than in nature. However, since in our simulations the $s$ quark has its physical mass, for hyperons this difference is reduced as strangeness decreases. Negative-parity states are typically about 500–600 MeV heavier than their partners, both in our simulations and in the PDG. Some negative-parity states in the PDG seem anomalously light, such as the $\Lambda(1405)$, and the status of this state is indeed under discussion (see e.g., the review [31] and references therein). In these cases, Table II also lists masses from the PDG which are separated by about 500 MeV and hence are potential candidates for parity partners, as suggested by our results at the lowest temperature (we note here that our spectroscopy methods are not specifically designed for high-precision spectroscopy in vacuum). As a final remark at the lowest temperature, we note that the positive-parity masses satisfy, to high precision, the Gell-Mann–Okubo mass relation [32,33]

$$\frac{3}{4}m_\Lambda + \frac{1}{4}m_\Sigma - \frac{1}{2}(m_N + m_\Xi) = 0,$$

for octet baryons and Gell-Mann’s equal spacing rule

$$m_{\Sigma'} - m_\Delta = m_\Xi - m_\Sigma = m_\Omega - m_\Xi$$

for decuplet baryons, also for our choice of quark masses, but the negative-parity masses do not (as is expected).

We now turn to the discussion of temperature effects, also presented in Table II and summarized in Figs. 1 and 2, where we show $m_{\pm}(T)$ in the various channels, normalized with $m_\pm$ at the lowest temperature, $T_0 = 44$ MeV. Several observations can be made. The positive-parity masses are largely temperature independent. A slight increase and subsequent drop when approaching the transition can be seen, but it is not significant within current errors. A corollary is that the relations (3), (4) are satisfied throughout the confined phase (within error), which constrains thermal model-building efforts. The negative-parity masses on the other hand drop in all channels in a similar way, and become near-degenerate with the corresponding positive-parity mass near the transition. The larger errors for the negative-parity states indicate that it is harder to fit the negative-parity correlators, impeding very precise statements about the degeneracy very close to the transition.
needed not coincide, a more elaborate Ansatz would replace
Since in a crossover the determination of a transition
masses remain approximately constant. We find this to be
e.g., the requirement that \( m_{-}(T_{c}) = m_{+}(T_{c}) \), i.e.,
the temperature at which the masses become degenerate.

Since there are only 4 data points in the confined phase and
the uncertainty is largest close to \( T_{c} \), we choose to
proceed here with the Ansatz (5), postponing to Sec. V
an estimate of \( T_{c}^{x} \) directly from the Euclidean correlators in
each channel.

Since the transition is a crossover rather than a real phase
transition, with the strength of the transition depending on
the masses of the light quarks, the fit parameter \( \gamma > 0 \) is
used to encode the width of the transition region, with small
(large) \( \gamma \) corresponding to a narrow (broad) crossover
region. We have carried out fits in each of the 8 channels and
find
\[
0.22 \lesssim \gamma \lesssim 0.35, \quad 0.85 \lesssim \frac{m_{-}(T_{c})}{m_{-}(0)} \lesssim 1.1. \tag{7}
\]

The largest uncertainty resides in \( m_{-}(T_{c}) \), since it assumes
that the concept of a well-defined ground state at or close to
\( T_{c} \) remains sensible. Note that in the fits we fixed
\( m_{-}(0) = m_{-}(T_{0}) \). The results of the fits are shown as
dashed lines in Figs. 1 and 2. We use the results of this
analysis in the next section.

To summarize, our results confirm that parity doubling
indeed emerges, as expected, and moreover establish that
the degeneracy develops from a reduction of the negative-
parity masses with temperature, while the positive-parity
masses remain approximately constant. We find this to be
similar in all the channels studied. While the emergence of
degeneracy is not surprising, the manner in which this is
realized cannot be determined from symmetry alone, but
requires a dynamical calculation, as we have done here. We
note that our findings can be used to constrain effective
parity-doublet models [34–36], in which a chirally invariant
component to baryon masses, denoted as \( m_{0} \), is introduced.
These models permit a nonzero baryon mass also when
chiral symmetry is restored, with the typical behavior of the
mass of parity partners being [34–37]

\[
m_{\pm} = \sqrt{m_{0}^{2} + c_{1} \sigma_{0}^{2} \mp c_{2} \sigma_{0}}, \tag{8}
\]

where \( \sigma_{0} \) denotes the chiral condensate in vacuum and
\( c_{1,2} \) are parameters related to the couplings between the baryons
and the light mesons. Incorporating medium effects by
allowing \( \sigma_{0} \) to be temperature dependent yields a prediction
for the temperature dependence of the baryon masses, but
some nontrivial interplay is to be expected to ensure that
\( m_{\pm} \) remains largely independent of temperature, as our data
indicates. Some recent work along these lines can be found
in Refs. [38–45] (see also Ref. [46] for an approach based on
the Faddeev kernel). Studies determining only the positive-
parity hyperon ground states at nonzero temperature include
Ref. [47] (using the Polyakov-Nambu-Jona-Lasinio (PNJL)
model) and Ref. [48] (using QCD sum rules).

To model the temperature dependence of \( m_{-}(T) \), we
have fitted the data with a simple Ansatz, interpolating
between \( m_{-}(0) \) and \( m_{-}(T_{c}) \),

\[
m_{-}(T) = w(T, \gamma)m_{-}(0) + [1 - w(T, \gamma)]m_{-}(T_{c}), \tag{5}
\]

Here

\[
w(T, \gamma) = \frac{\tanh \left[ \frac{1}{\gamma^{-1}} - \frac{T - T_{c}}{T_{c}} \right]}{\tanh \left( \frac{1}{\gamma^{-1}} \right)} \tag{6}
\]

is a transition function, with \( w(0, \gamma) = 1 \) and \( w(T_{c}, \gamma) = 0 \).

Since in a crossover the determination of a transition
This is shown in Figs. 1 and 2.

FIG. 1. Temperature dependence of the ground state masses,
normalized with \( m_{-} \) at the lowest temperature, \( m_{-}(T)/m_{-}(T_{0}) \),
in the hadronic phase, for octet baryons. Positive- (negative-)
parity masses are indicated with open (closed) symbols.

FIG. 2. As above, for decuplet baryons.
IV. IN-MEDIUM HADRON RESONANCE GAS

We now consider a possible application of our findings in the confined phase, which has relevance for heavy-ion phenomenology. A widely used model to describe thermodynamical properties of QCD at low temperature is the hadron resonance gas (HRG), in which all resonances identified in the PDG contribute to the pressure and other thermodynamic quantities, such as generalized susceptibilities. In the standard formulation, the resonances are not interacting and their properties are taken as in vacuum, i.e., not affected by the presence of a (thermal) medium. This ideal HRG gives a reasonable description of experimental and lattice QCD data, but discrepancies appear at a quantitative level. As mentioned in the Introduction, several modifications of the HRG have been proposed to cure this [10–12]. Since the ideal HRG results typically fall below e.g., the lattice QCD data for thermodynamic quantities, it has been proposed to include more states than have been identified in the PDG, since this will result in an increase of the pressure and of susceptibilities. Indeed, including states which appear in the quark model but have not (yet) been identified experimentally leads to a better agreement between lattice data and this extended HRG [8,9,13].

Motivated by our findings above, we propose here to include medium effects in the hadronic masses, rather than keeping them as in vacuum. Since we observed that the negative-parity ground state masses drop as the temperature increases, we can anticipate an increase in the pressure and of susceptibilities. Hence a qualitative improvement is expected. We will refer to this proposal as the in-medium HRG, to distinguish it from other modifications. Since in this paper we are concerned with spectral changes for baryons, we apply the in-medium HRG to quantities that are sensitive to baryon number, namely the baryonic contributions to the pressure and the correlation between baryon number and strangeness,

$$\chi_{BS} = \frac{1}{VT} \langle BS \rangle = \frac{T}{V} \frac{\partial^2 \ln Z}{\partial \mu_B \partial \mu_S},$$

where $V$ is the spatial volume and $Z$ the partition function.

Let us now turn to the concrete implementation. As supported by the lattice study, positive-parity masses are kept fixed, i.e., at their vacuum value, but the negative-parity ground state masses are taken to be temperature dependent, according to the prescription (5). We do not modify masses of excited states, as we have currently no predictions for their temperature dependence from the lattice, but one could envision including this. Our lattice study was carried out using two light flavors which are heavier than in nature. In our in-medium HRG application, we use the actual mass values given in the PDG: concretely, we use the PDG2016 baryon masses classified with 3 and 4 stars, up to 2.5 GeV. In the case that there are several candidates for negative-parity partners—e.g., $\Lambda(1450)$ and $\Lambda(1670)$—we have identified as parity partners the ones that are separated by about 500–600 MeV, i.e., $\Lambda(1670)$, $\Sigma(1940)$ and $\Xi(1950)$, similar as for the other baryons. For the pseudocritical temperature, we used $T_c = 155$ MeV, which is determined by chiral observables [6,49]. The strength of the transition is expected to depend on the masses of the light flavors. To incorporate this, we have varied the parameter $\gamma$ encoding the width of the transition region, see Eq. (5), but have found no effect within the uncertainty arising from varying $m_-(T_c)/m_+(0)$. For the results shown in Figs. 3 and 4, we have used $\gamma = 0.3$ and varied the ratio $m_-(T_c)/m_+(0)$ between 1 and 1.1.
In Fig. 3, we show the dimensionless combination $-\chi_{BS}/T^2 = -(BS)/VT^3$, representing fluctuations of strange baryons. The standard HRG result, shown by the full line, lies below the continuum-extrapolated lattice data from the Budapest-Wuppertal collaboration [50–52]. The in-medium HRG result moves away from the HRG line as the temperature increases, since a subset of the strange baryons becomes lighter as the system heats up, in qualitative agreement with the lattice data. Within the uncertainty, which is dominated by the variation of $m_-(T_0)/m_+(0)$, we find that the in-medium HRG result agrees with the lattice data also quantitatively.

Figure 4 shows the contributions to the normalized pressure $p/T^4$ from the sectors with baryon number $|B| = 1$, organized by strangeness. The ideal and in-medium HRG are compared to the lattice data of Refs. [9,53]. In the $S = 0$ sector, the ideal HRG describes the data very well and in fact modifications of the HRG will typically make the comparison worse. In the $|S| = 1, 2, 3$ sectors, however, the standard HRG lies significantly below the lattice data. Here we observe that the in-medium HRG leads to a quantitative improvement.

To conclude, a few comments are in order. First we note that both mesons and baryons enter in the HRG and for many thermodynamic quantities mesons, containing the lightest states, dominate. In our lattice study, we have considered baryons only. Hence in the application above we have consider quantities that are sensitive to baryon number. To extend the in-medium HRG to include mesonic resonances requires a detailed study the mesonic spectrum as the temperature increases, which we leave for the future. Second, with temperature-dependent masses, an application of the in-medium HRG to thermodynamic quantities which are obtained as temperature derivatives of the pressure, such as the entropy density $s = \partial p/\partial T$, care has to be taken to be thermodynamically consistent, see e.g., Ref. [54]. Finally, given that there are a number of HRG modifications which aim to improve the ideal HRG in complementary ways, it would be interesting to consider various modifications simultaneously, provided they are not in incompatible on physical grounds.

V. PARITY DOUBLING

We now return to the lattice data and analyse the transition from the hadronic phase to the quark-gluon plasma, in particular the emergence of parity doubling.

At $T = 201$ MeV ($T/T_c = 1.09$), the lowest temperature in the deconfined phase we have access to, we find that clearly identifiable bound states do not appear to be present; evidence in the $N$ and $\Omega$ channels has already been reported in Ref. [17]. Instead, we study the emergence of parity doubling, which can be done directly at the level of the correlators $G_{\pm}$, without the need for identifiable ground states. We consider the ratio [20,21]

$$R(\tau) = \frac{G_+(\tau) - G_+(1/T - \tau)}{G_+(\tau) + G_+(1/T - \tau)},$$

(10)
to analyze the difference between the channels with opposite parity, see Eq. (2). Note that we consider zero momentum only and hence drop the $p$ dependence. In the case of parity doubling, $G_+(\tau) = G_+(1/T - \tau) = -G_-(\tau)$ and $R(\tau) = 0$. In absence of parity doubling, and in the presence of clearly separated ground states with a gap between the positive- and negative-parity ground states, such that

$$G_\pm(\tau) \sim \pm A_\pm e^{-m_\pm \tau}, \quad m_\pm \gg m_+,$$

(11)
one finds that $R(\tau) = 1$, in the interval where the ground states dominate [17,20,21]. We can capture this in a single quantity $R$ by summing over the temporal lattice points,

$$R = \frac{\sum_n R(\tau_n)/\sigma^2(\tau_n)}{\sum_n 1/\sigma^2(\tau_n)},$$

(12)
where $\sigma(\tau_n)$ denotes the error at time slice $\tau_n$ and $4 \leq n \leq N_\tau / 2 - 1$, to exclude lattice artefacts and excited states present at early times. (Note that the same procedure was followed in Refs. [17,21]; the starting value in the sums in Refs. [17,21] was incorrectly given as $n = 1$.) If the Ansatz of a single exponential at low temperature, Eq. (11), describes the data well, one finds that the quasiorder parameter $R$ equals 1, while it vanishes in the case of parity doubling.

The results for $R$ as a function of temperature are shown in Fig. 5. Note that the channels are identified by the parity $S$, $N$, $\Delta$, $\Sigma$, $\Lambda$, $\Xi$, $\Omega$, $\Xi^*$

![Figure 5](https://example.com/fig5.png)

FIG. 5. Crossover behavior of $R$, see Eqs. (10), (12), as a function of temperature and ordered by strangeness, indicating the emergence of parity doubling in the deconfined phase. The grey lines are cubic spline fits, with the width indicating a statistical uncertainty only. The vertical lines indicate the transition temperature extracted from the renormalized Polyakov loop, $T_c = 185(4)$ MeV.
particle content and are ordered by strangeness. We note that $R$ indeed changes from (close to) 1 to (close to) 0 as $T$ increases, with the crossover taking place in the transition region as determined by the Polyakov loop. At the highest temperatures, the difference from 0 appears directly proportional to the number of strange quarks in the channel, which reflects the explicit chiral symmetry breaking arising from the heavier strange quark. Eventually, this effect should disappear as $m_s/T \to 0$. We hence conclude that the interpretation of parity doubling due to chiral symmetry restoration in the baryon sector is indeed valid.

When the transition between two phases is not a phase transition but merely an analytic crossover, as is the case for the thermal transition in QCD [55], a single transition temperature cannot be given. Instead one finds a range of transition or pseudocritical temperatures, which depend on the observable and method used to define it, see e.g., Ref. [6] and references therein. In Sec. III we denoted the transition temperature linked to parity doubling as $T_\chi$, but did not determine it. Here we will estimate it directly from the $R$ ratio. An often used method is to locate the inflection point of (quasi)order parameters. For this reason, we have fitted cubic splines to the lattice data in Fig. 5, which are represented by the grey lines, with the widths giving an indication of the statistical error. Using the cubic splines, we have extracted the temperatures of the inflection points, which are shown in Fig. 6, organized by strangeness and labeled by the ground state of the respective channels. The errors are statistical only and are determined by the bootstrap method. The transition temperature determined from the renormalized Polyakov loop, $T_c = 185(4)$ MeV, is indicated by the shaded band. We observe that the inflection-point temperatures lie below this band, by about 9 to 15 MeV (the result in the $\Sigma$ channel lies somewhat lower than expected, see also Fig. 5). Due to the crossover nature of the transition, this is not unexpected. A possible dependence on strangeness (see e.g., Ref. [56] on flavor separation during the crossover) might become better visible when the light quarks are tuned closer to their physical values. This project is currently in progress [57].

VI. SUMMARY

In this paper we determined the response of hyperons to an increase of temperature in thermal QCD, going from the hadronic phase to the quark-gluon plasma, using lattice QCD simulations. While the masses of the positive-parity ground states were seen to be not affected, within the numerical uncertainty, the masses of the negative-parity ground states showed a characteristic temperature dependence, in all channels. We have argued that both findings are relevant for the phenomenology of heavy-ion collisions, in particular in the context of the hadron resonance gas. We have formulated an in-medium HRG to incorporate the temperature dependence of the negative-parity ground states and applied it to fluctuations involving strange baryons and baryonic contributions to the pressure, which had been computed independently on the lattice. While in the nucleon and $\Delta$ ($S = 0$) channels the standard HRG describes the lattice data already very well (and any modification makes the comparison worse), we found that for hyperons the in-medium HRG leads to an improved agreement between lattice QCD results for those quantities and the HRG. It would therefore be interesting to extend this approach to mesons as well and determine the temperature dependence of spectral features of mesons. This work is currently in progress. Besides this, it would be of interest to combine our suggestion for the in-medium HRG with other modifications of the ideal HRG, to be able to study how various modifications may work together. Finally, our results in the hadronic phase can also be used to benchmark effective models, such as parity doublet and PNJL-type models.

At the higher temperatures, proceeding into the quark-gluon plasma, we focused on the emergence of parity doubling, at the level of the correlators. We defined an $R$ ratio, which captures the transition from the chirally broken to the chirally symmetric phase. The temperatures of the inflection points of this $R$ ratio lie somewhat below the pseudocritical temperature extracted from the Polyakov loop, indicating the crossover nature of the transition. To observe possible strangeness dependence, a larger separation between the strange and light quark masses would be advantageous. This would also allow us to further study modifications to the hadronic spectrum in the low-temperature phase, closer to the physical point. Work in this direction is currently underway.
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[1] R. Dashen, S. K. Ma, and H. J. Bernstein, S Matrix formulation of statistical mechanics, Phys. Rev. 187, 345 (1969).
[2] R. Venugopalan and M. Prakash, Thermal properties of interacting hadrons, Nucl. Phys. A546, 718 (1992).
[3] F. Karsch, K. Redlich, and A. Tawfik, Hadron resonance mass spectrum and lattice QCD thermodynamics, Eur. Phys. J. C 29, 549 (2003).
[4] A. Andronic, P. Braun-Munzinger, and J. Stachel, Hadron production in central nucleus-nucleus collisions at chemical freeze-out, Nucl. Phys. A772, 166 (2006).
[5] A. Andronic, P. Braun-Munzinger, K. Redlich, and J. Stachel, Decoding the phase structure of QCD via particle production at high energy, Nature (London) 561, 321 (2018).
[6] S. Borsányi, Z. Fodor, C. Hoelbling, S. D. Katz, S. Krieg, C. Ratti, and K. K. Szabó (Wuppertal-Budapest Collaboration), Is there still any $T_c$ mystery in lattice QCD? Results with physical masses in the continuum limit III, J. High Energy Phys. 09 (2010) 073.
[7] A. Bazavov et al. (HotQCD Collaboration), Equation of state in (2 + 1)-flavor QCD, Phys. Rev. D 90, 094503 (2014).
[8] A. Bazavov et al., Additional Strange Hadrons from QCD Thermodynamics and Strangeness Freezeout in Heavy Ion Collisions, Phys. Rev. Lett. 113, 072001 (2014).
[9] P. Alba et al., Constraining the hadronic spectrum through QCD thermodynamics on the lattice, Phys. Rev. D 96, 034517 (2017).
[10] V. Vovchenko, M. I. Gorenstein, and H. Stoecker, van der Waals Interactions in Hadron Resonance Gas: From Nuclear Matter to Lattice QCD, Phys. Rev. Lett. 118, 182301 (2017).
[11] P. Huovinen and P. Petreczky, Hadron Resonance Gas with Repulsive Interactions and Fluctuations of Conserved Charges, Phys. Lett. B 777, 125 (2018).
[12] L. M. Satarov, V. Vovchenko, P. Alba, M. I. Gorenstein, and H. Stoecker, New scenarios for hard-core interactions in a hadron resonance gas, Phys. Rev. C 95, 024902 (2017).
[13] A. Majumder and B. Müller, Hadron Mass Spectrum from Lattice QCD, Phys. Rev. Lett. 105, 252002 (2010).
[14] G. E. Brown and M. Rho, Chiral restoration in hot and/or dense matter, Phys. Rep. 269, 333 (1996).
[15] R. Rapp and J. Wambach, Chiral symmetry restoration and dileptons in relativistic heavy ion collisions, Adv. Nucl. Phys. 25, 1 (2000).
[16] P. Braun-Munzinger, J. Stachel, and C. Wetterich, Chemical freezeout and the QCD phase transition temperature, Phys. Lett. B 596, 61 (2004).
[17] G. Aarts, C. Allton, D. De Boni, S. Hands, B. Jäger, C. Praki, and J. I. Skullerud, Light baryons below and above the deconfinement transition: medium effects and parity doubling, J. High Energy Phys. 06 (2017) 034.
[18] C. E. Detar and J. B. Kogut, The Hadronic Spectrum of the Quark Plasma, Phys. Rev. Lett. 59, 399 (1987); Measuring the Hadronic Spectrum of the Quark Plasma, Phys. Rev. D 36, 2828 (1987).
[19] I. Pushkina, P. de Forcrand, M. Garcia Perez, S. Kim, H. Matsufuru, A. Nakamura, I-O. Stamatescu, T. Takaishi, and T. Umeda (QCD-TARO Collaboration), Properties of hadron masses at finite baryonic density, Phys. Lett. B 609, 265 (2005).
[20] S. Datta, S. Gupta, M. Padmanath, J. Maiti, and N. Mathur, Nucleons near the QCD deconfinement transition, J. High Energy Phys. 02 (2013) 145.
[21] G. Aarts, C. Allton, S. Hands, B. Jäger, C. Praki, and J. I. Skullerud, Nucleons and parity doubling across the deconfinement transition, Phys. Rev. D 92, 014503 (2015).
[22] G. Aarts, C. Allton, T. Harris, S. Kim, M. P. Lombardo, S. M. Ryan, and J. I. Skullerud, The bottomonium spectrum at finite temperature from $N_L = 2 + 1$ lattice QCD, J. High Energy Phys. 07 (2014) 097.
[23] G. Aarts, C. Allton, A. Amato, P. Giudice, S. Hands, and J. I. Skullerud, Electrical conductivity and charge diffusion in thermal QCD from the lattice, J. High Energy Phys. 02 (2015) 186.
[24] G. Aarts, C. Allton, D. De Boni, S. Hands, B. Jäger, C. Praki, and J. I. Skullerud, Medium effects and parity doubling of hyperons across the deconfinement phase transition, EPJ Web Conf. 175, 07016 (2018); Baryons in the plasma: in-medium effects and parity doubling, EPJ Web Conf. 171, 14005 (2018).
[25] R. G. Edwards, B. Joo, and H. W. Lin, Tuning for Three-flavors of Anisotropic Clover Fermions with Stout-link Smearing, Phys. Rev. D 78, 054501 (2008).

[26] C. Morningstar and M. J. Peardon, Analytic smearing of SU(3) link variables in lattice QCD, Phys. Rev. D 69, 054501 (2004).

[27] A. Amato, G. Aarts, C. Allton, P. Giudice, S. Hands, and J. I. Skullerud, Electrical Conductivity of the Quark-Gluon Plasma Across the Confinement Transition, Phys. Rev. Lett. 111, 172001 (2013).

[28] A. Kelly, A. Rothkopf, and J. I. Skullerud, Bayesian study of relativistic open and hidden charm in anisotropic lattice QCD, Phys. Rev. D 97, 114509 (2018).

[29] S. Güsken, U. Löw, K. H. Mütter, R. Sommer, A. Patel, and K. Schilling, Nonsinglet Axial Vector Couplings of the Baryon Octet in Lattice QCD, Phys. Lett. B 227, 266 (1989).

[30] M. Tanabashi et al. (Particle Data Group), Review of particle physics, Phys. Rev. D 98, 030001 (2018).

[31] T. Hyodo and D. Jido, The nature of the Λ(1405) resonance in chiral dynamics, Prog. Part. Nucl. Phys. 67, 55 (2012).

[32] M. Gell-Mann, The eightfold way: A theory of strong interaction symmetry, USDOE, Reports No. CTSL-20 and No. TID-12608, 1961.

[33] S. Okubo, Note on unitary symmetry in strong interactions, Prog. Theor. Phys. 27, 949 (1962).

[34] C. E. Detar and T. Kunihiro, Linear σ model with parity doubling, Phys. Rev. D 39, 2805 (1989).

[35] D. Jido, T. Hatsuda, and T. Kunihiro, Chiral Symmetry Realization for Even Parity and Odd Parity Baryon Resonances, Phys. Rev. Lett. 84, 3252 (2000).

[36] D. Jido, M. Oka, and A. Hosaka, Chiral symmetry of baryons, Prog. Theor. Phys. 106, 873 (2001).

[37] J. Steinheimer, S. Schramm, and H. Stöcker, The hadronic SU(3) Parity Doublet Model for Dense Matter, its extension to quarks and the strange equation of state, Phys. Rev. C 84, 045208 (2011).

[38] S. Benic, I. Mishustin, and C. Sasaki, Effective model for the QCD phase transitions at finite baryon density, Phys. Rev. D 91, 125034 (2015).

[39] Y. Motohiro, Y. Kim, and M. Harada, Asymmetric nuclear matter in a parity doublet model with hidden local symmetry, Phys. Rev. C 92, 025201 (2015); 95, 059903(E) (2017).

[40] H. Nishihara and M. Harada, Extended Goldberger-Treiman relation in a three-flavor parity doublet model, Phys. Rev. D 92, 054022 (2015).

[41] D. Suenaga, Examination of N′ (1535) as a probe to observe the partial restoration of chiral symmetry in nuclear matter, Phys. Rev. C 97, 045203 (2018).

[42] Y. Takeda, Y. Kim, and M. Harada, Catalysis of partial chiral symmetry restoration by Δ matter, Phys. Rev. C 97, 065202 (2018).

[43] A. Mukherjee, S. Schramm, J. Steinheimer, and V. Dexheimer, The application of the Quark-Hadron Chiral Parity-Doublet Model to neutron star matter, Astron. Astrophys. 608, A110 (2017).

[44] C. Sasaki, Parity doubling of baryons in a chiral approach with three flavors, Nucl. Phys. A970, 388 (2018).

[45] T. Yamazaki and M. Harada, Chiral partner structure of light nucleons in an extended parity doublet model, Phys. Rev. D 99, 034012 (2019).

[46] C. Chen, B. El-Bennich, C. D. Roberts, S. M. Schmidt, J. Segovia, and S. Wan, Structure of the nucleon’s low-lying excitations, Phys. Rev. D 97, 034016 (2018).

[47] J. M. Torres-Rincon, B. Sintes, and J. Aichelin, Flavor dependence of baryon melting temperature in effective models of QCD, Phys. Rev. C 91, 065206 (2015).

[48] K. Azizi and G. Bozkr, Decuplet baryons in a hot medium, Eur. Phys. J. C 76, 521 (2016).

[49] A. Bazavov et al., The chiral and deconfinement aspects of the QCD transition, Phys. Rev. D 85, 054503 (2012).

[50] S. Borsányi, Z. Fodor, S. D. Katz, S. Krieg, C. Ratti, and K. Szabo, Flouctuations of conserved charges at finite temperature from lattice QCD, J. High Energy Phys. 01 (2012) 138.

[51] R. Bellwied, S. Borsányi, Z. Fodor, S. D. Katz, A. Pasztor, C. Ratti, and K. K. Szabo, Fluctuations and correlations in high temperature QCD, Phys. Rev. D 92, 114505 (2015).

[52] S. Borsányi (private communication).

[53] C. Ratti (private communication).

[54] P. Levai and U. W. Heinz, Massive gluons and quarks and the equation of state obtained from SU(3) lattice QCD, Phys. Rev. C 57, 1879 (1998).

[55] Y. Aoki, G. Endrodi, Z. Fodor, S. D. Katz, and K. K. Szabo, The Order of the quantum chromodynamics transition predicted by the standard model of particle physics, Nature (London) 443, 675 (2006).

[56] R. Bellwied, S. Borsányi, Z. Fodor, S. D. Katz, and C. Ratti, Is There a Flavor Hierarchy in the Deconfinement Transition of QCD?, Phys. Rev. Lett. 111, 202302 (2013).

[57] G. Aarts, C. Allton, J. Glesaaen, S. Hands, B. Jäger, and J. Skullerud, Hadronic spectrum calculations in the quark-gluon plasma, arXiv:1812.08151.