A Controlled Study of Cold Dust Content in Galaxies from $z = 0–2$

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Abstract

At $z = 1–3$, the formation of new stars is dominated by dusty galaxies whose far-IR emission indicates they contain colder dust than local galaxies of a similar luminosity. We explore the reasons for the evolving IR emission of similar galaxies over cosmic time using (1) local galaxies from GOALS ($L_{\text{IR}} = 10^{11}$–$10^{12} L_\odot$), (2) galaxies at $z \sim 0.1–0.5$ from 5MUSES ($L_{\text{IR}} = 10^{10}$–$10^{12} L_\odot$), and (3) IR luminous galaxies spanning $z = 0.5–3$ from GOODS and Spitzer xFLS ($L_{\text{IR}} > 10^{11} L_\odot$). All samples have Spitzer mid-IR spectra, and Herschel and ground-based submillimeter imaging covering the full IR spectral energy distribution, allowing us to robustly measure $L_{\text{IR}}$, $T_{\text{dust}}$, and $M_{\text{dust}}$ for every galaxy. Despite similar infrared luminosities, $z > 0.5$ dusty star-forming galaxies (DSFGs) have a factor of 5 higher dust masses and 5 K colder temperatures. The increase in dust mass is linked to an increase in the gas fractions with redshift, and we do not observe a similar increase in stellar mass or star formation efficiency. $L_{\text{SF}}(50)/L_{\text{IR}}$, a proxy for $T_{\text{dust}}$, is strongly correlated with $L_{\text{IR}}/M_{\text{dust}}$ independently of redshift. We measure merger classification and galaxy size for a subsample, and there is no obvious correlation between these parameters and $L_{\text{IR}}/M_{\text{dust}}$. In DSFG, the change in $L_{\text{IR}}/M_{\text{dust}}$ can fully account for the observed colder dust temperatures, suggesting that any change in the spatial extent of the interstellar medium is a second-order effect.

Key words: galaxies: fundamental parameters – galaxies: high-redshift – galaxies: ISM – galaxies: star formation

1. Introduction

As the universe ages, a phenomenon known as cosmic downsizing shifts the bulk of star formation to smaller galaxies. Additionally, as the universe expands, the merger rate of galaxies decreases, and mergers become a less important triggering mechanism for star formation (Conselice et al. 2008, 2009; Bluck et al. 2012). These changes mean that, in certain respects, the composition of galaxies in the local universe is quite different from what we would see if we existed in a galaxy at cosmic noon, 8–10 billion years ago ($z = 1–2$), when the universe was forming most of its stars (Madau & Dickinson 2014). Galaxies at cosmic noon appear to be more compact than their present-day counterparts of similar mass (e.g., Trujillo et al. 2007; van Dokkum et al. 2008; Williams et al. 2014), suggesting that the inner parts of galaxies are in place before the outer parts form (e.g., Hopkins et al. 2009; Nelson et al. 2016).

On the other hand, the cosmic noon universe shares some key similarities with our present-day universe. For example, the backbone of the Hubble sequence was already in place by $z \sim 2$, so that blue, disky galaxies were strongly star forming (e.g., Lee et al. 2013). Crucially, the main sequence of galaxy formation already existed by $z \sim 3$ (e.g., Behroozi et al. 2013; Suzuki et al. 2015). The main sequence is the tight empirical relationship between SFR and $M_*$ that defines the so-called “normal mode” of secular star formation, as opposed to short-lived intense starbursts, typically triggered by mergers (e.g., Brinchmann et al. 2004; Noeske et al. 2007; Elbaz et al. 2011).

At cosmic noon, the galaxies dominating the buildup of stellar mass are massive, dusty, infrared luminous systems ($L_{\text{IR}} > 10^{11} L_\odot$), but today, less massive, relatively isolated galaxies such as our Milky Way are the dominant sites of star formation (Murphy et al. 2011; Madau & Dickinson 2014; Martis et al. 2016). IR luminous galaxies exist in the local universe as well, but they contribute little to the current cosmic SFR density. Historically, galaxy IR spectral energy distributions (SEDs) were parameterized only by $L_{\text{IR}}$ (Sanders & Mirabel 1996; Chary & Elbaz 2001; Dale et al. 2001; Rieke et al. 2009). However, Herschel brought new insight into the peak of the SED in distant galaxies, and we now know that at $z \sim 1–2$, ultra-luminous infrared galaxies (ULIRGs) have colder far-IR emission than galaxies with the same luminosity at $z \sim 0$.
The shape of the ULIRG SED evolves strongly from \( z \approx 0 \rightarrow 2 \), but local ULIRGs represent the most extreme objects. They are merging, compact starbursts, which are heavily obscured and even optically thick at far-IR wavelengths (e.g., Sakamoto et al. 2008; Scoville et al. 2015). These objects also lie well above the main sequence, while ULIRGs at \( z \approx 1 \rightarrow 2 \) lie on the main sequence, indicative of a slower, secular star formation history (Elbaz et al. 2011). However, local LIRGs, which are an order of magnitude less luminous than local ULIRGs, share certain dust emission characteristics with their high-redshift luminosity-based counterparts, indicating they may have similar ISMs despite the fact that local LIRGs also lie above the main sequence. For example, \( z \approx 1 \rightarrow 2 \) ULIRGs and LIRGs have similar polycyclic aromatic hydrocarbon (PAH) emission strength, parameterized by 6.2 \( \mu m \) equivalent widths and \( L_{6.2}/L_{IR} \), as local LIRGs (Pope et al. 2013; Kirkpatrick et al. 2014b; Stierwalt et al. 2014). The similarity of these features indicates a similar photodissociation region structure in these galaxies, hinting at similarities between their interstellar media (Papovich et al. 2009; Pope et al. 2013; Stierwalt et al. 2014). Therefore, despite the evolution of the main sequence with lookback time, it is reasonable to examine how closely dusty galaxies resemble each other from \( z = 0 \rightarrow 2 \).

Far-IR/submillimeter emission is sensitive to dust temperature, emissivity, dust mass, the geometry of the star-forming regions within the ISM, and the incident radiation field (Witt & Gordon 2000; Gordon et al. 2001; Misselt et al. 2001), although the far-IR SED is most commonly used to calculate three parameters: \( L_{IR}(8\rightarrow1000 \mu m) \); \( M_{dust} \), measured from the Rayleigh–Jeans tail; and \( T_{dust} \), which characterizes the peak of the SED. The change of SED shape, along with the similarity and differences between the distant and local universe, leads to a key question in galaxy evolution: what is the root cause of the colder dust emission at \( z \approx 1 \rightarrow 2 \)?

Recently, it has been suggested that \( L_{IR} \) and ISM geometry (including surface density and compactness) fully account for the shape of the SED; that is, high-redshift IR luminous galaxies are colder because they are more extended (Elbaz et al. 2011; Rujopakarn et al. 2013). Additionally, the overall structure of the ISM in high-redshift galaxies may be different—a larger fraction of gas is likely in H\(_2\) rather than H\(_{\text{II}}\), the mass function of giant molecular clouds evolves, and proportionally more of the dust may arise from the diffuse ISM in distant galaxies (Popping et al. 2014a, 2014b; Scoville et al. 2016). However, theoretical simulations and radiative transfer calculations contend that \( L_{IR} \) and \( M_{dust} \) or total mass, \( M \), are the primary parameters for determining a galaxy’s global SED (Chakrabarti & McKee 2005; Safarzadeh et al. 2016). Then, the compactness of the ISM, mass function of molecular clouds, and possibly surface density have second-order effects over the shape of the SED. Indeed, Lee et al. (2016) demonstrate at \( z = 0 \) that heavily dust-obscured galaxies with \( L_{IR} = 10^{11} \rightarrow 10^{12} L_{\odot} \) have similar dust masses and temperatures as their less obscured counterparts, even though the extremely dust-obscured galaxies are likely much more compact. This would suggest that the geometry of the ISM in IR luminous galaxies has little overall effect on the measured dust mass and temperature.

In this work, we test how the dust temperatures and dust masses change with \( L_{IR} \) and redshift for IR luminous galaxies from \( z \sim 0 \rightarrow 2 \). We utilize three extensively studied samples from the literature, which are large (\( \gtrsim 200 \) galaxies in each sample) and have deep multiwavelength data sets that eliminate any need for photometric stacking. We analyze all the SEDs in a self-consistent manner. Crucially, all of our galaxies have mid-IR spectroscopy, which we use to remove active galactic nuclei (AGNs) and compact starbursts, excluding a potential source of uncertainty when comparing dust masses and temperatures (e.g., Lee et al. 2016). In Section 2, we describe our three data sets and summarize the relevant literature pertaining to these samples; in Section 3, we discuss how we remove AGNs and measure dust masses self-consistently; in Section 4, we characterize the shape of the far-IR SED using broadband colors; in Section 5, we measure an increase in the dust mass of dusty star-forming galaxies (DSFGs) with redshift and parameterize the relationship between \( L_{IR}/M_{dust} \) and \( T_{dust} \); in Section 6, we discuss the origin of the increased dust masses with redshift and whether ISM size or merger classification can influence the SED; and we summarize in Section 7. Throughout this work, we assume a flat cosmology with \( H_0 = 70 \text{ km s}^{-1}\text{Mpc}^{-1} \), \( \Omega_M = 0.3 \), and \( \Omega_\Lambda = 0.7 \).

2. Sample Description

In this study, we compare the far-IR/submillimeter properties of three samples at different redshifts extensively described in the literature (Figure 1): (1) \( z < 0.088 \): Great Observatories All Sky Survey (GOALS; PI L. Armus, Armus et al. 2009); (2) \( z = 0.05 \rightarrow 0.75 \): 5 mJy Unbiased Spitzer Extragalactic Survey (5MUSES; P. I. G. Helou, Wu et al. 2010); and (3) \( z = 0.3 \rightarrow 3.0 \): the Spitzer IRS Supersample (Kirkpatrick et al. 2013b). These samples comprise a case study of dusty star-forming galaxies where the far-IR SEDs are well sampled and stacking is not required. Indeed, these samples are ideal for comparison as they each contain massive (\( M_\phi \gtrsim 10^9 M_\odot \)), infrared luminous (\( L_{IR} = 10^{10} \rightarrow 10^{12} L_\odot \)) galaxies with far-IR imaging from the Spitzer Space Telescope and the Herschel Space Observatory, and mid-IR spectroscopy from the Spitzer IRS instrument (Houck et al. 2004), useful for quantifying and removing dust heating due to an obscured AGN. We briefly summarize the basic properties of each sample in the following subsections, and in Section 3, we discuss how we arrive at the final sample sizes of 46 galaxies from GOALS, 30 galaxies from 5MUSES, and 51 galaxies from the Supersample.

2.1. GOALS

The GOALS sample comprises 180 luminous IR galaxies (LIRGs; \( L_{IR} = 10^{11} L_\odot \)) and 22 ULIRGs (\( L_{IR} > 10^{12} L_\odot \)). Many of these systems are interacting, resulting in 244 individual galactic nuclei with Spitzer IRS spectroscopy. These galaxies are a representative subset of the IRAS Bright Galaxy Survey (Sanders et al. 2003) and were selected to have \( S_{60} > 5.24 \) Jy. GOALS sources cover the distance range 15 Mpc < \( D < 400 \) Mpc, which corresponds to \( z < 0.088 \).

The IRS spectra have been previously analyzed in depth (Díaz-Santos et al. 2010a, 2010b; U et al. 2012; Stierwalt et al. 2014). Here, we make use of the IRS SL staring observations, \( \lambda = 5.5 \rightarrow 14.5 \mu m \), to identify and remove AGNs from the sample (Section 3.1). The GOALS galaxies have global flux
dust masses from all three Spitzer MIPS bandpasses (J. Mazzarella et al. 2017, in preparation). $L_{\text{IR}}(8–1000 \mu \text{m})$ was calculated following the formula in Sanders & Mirabel (1996) using all four IRAS flux densities (Díaz-Santos et al. 2010a).

The UV-IR SEDs were analyzed in detail for a subset of 64 galaxies (see U et al. 2012 for a discussion of the selection of these objects). These galaxies have stellar mass measurements, so they form our initial dust mass sample as well. From the 64 galaxies, 58 sources have either 850 or 250 μm photometry from the James Clerk Maxwell Telescope or 250 μm photometry from Herschel (Chu et al. 2017), which we use to calculate $M_{\text{dust}}$. Five of these are double nuclei sources that we remove, and seven are hosting an AGN. This leaves a final sample size of 46 galaxies.

2.2. 5MUSES

5MUSES is a Spitzer IRS mid-IR spectroscopic survey of 330 galaxies selected from the SWIRE and Spitzer Extragalactic First Look Survey fields (details in Wu et al. 2010). It is a flux-limited sample selected at 24 μm, with $S_{24} > 5$ mJy. Two hundred and eighty sources have optical spectroscopic redshifts (Wu et al. 2010). 5MUSES is a representative sample of galaxies at intermediate redshift (the median redshift of the sample is 0.14) with $L_{\text{IR}} \sim 10^{10}$–$10^{12} L_{\odot}$, bridging the gap between local (U)LIRGs and high-redshift observations.

For the present study, we make use of the Spitzer IRS SL spectroscopy to quantify AGN emission. Complete details of the Spitzer data reduction are found in Wu et al. (2010). IRS spectra combined with Spitzer MIPS imaging is used to calculate $L_{\text{IR}}(5–1000 \mu \text{m})$ in Wu et al. (2010), with a slightly different cosmology ($\Omega_M = 0.27, \Lambda = 0.73$). We adjust the published $L_{\text{IR}}$ by multiplying by 0.99 to account for the difference in cosmology and 0.95 to scale to $L_{\text{IR}}(8–1000 \mu \text{m})$, which we have determined using a purely star-forming template from Kirkpatrick et al. (2013b). We use Herschel SPIRE observations of a subset of 188 sources in the Herschel Multi-Tiered Extragalactic Survey (HerMES; Oliver et al. 2010, 2012; Magdis et al. 2013) to calculate $M_{\text{dust}}$.

Of the 188 Herschel galaxies, 40 have 500 μm detections, necessary to calculate $M_{\text{dust}}$. Six of these are removed because they host an AGN. We remove an additional four sources where the 500 μm photometry appears blended with a nearby source. This leaves a final sample of 30 galaxies.

2.3. Supersample

We have assembled a multiwavelength data set for a sample of 343 high-redshift ($z \sim 0.3–4.0$) (U)LIRGs in the Great Observatories Origins Deep Survey North (GOODS-N), Extended Chandra Deep Field Survey (ECDFS), and Spitzer xFLS fields. All sources are selected to have mid-IR spectroscopy from Spitzer IRS, which is used to measure the redshift (Kirkpatrick et al. 2012). Our sample contains a range of sources from individual observing programs, each with differing selection criteria. However, the overarching selection criterion is a 24 μm flux limit of 0.9 mJy for the xFLS galaxies, which are taken from a shallower survey, and 0.1 mJy for the GOODS and ECDFS galaxies, compiled from a deep survey. In addition to IRS spectra, these sources all have Spitzer MIPS, and Herschel PACS and SPIRE imaging (Sajina et al. 2012; Kirkpatrick et al. 2013b). We calculate individual $L_{\text{IR}}(8–1000 \mu \text{m})$ by fitting a full suite of Spitzer and Herschel photometry with the library of templates from Kirkpatrick et al. (2013b). Redshifts are determined by fitting the main PAHs.
emission features, or by using optical spectroscopy in the case of a featureless MIR spectrum.

In this work, we also utilize 870 \( \mu \)m photometry of GOODS-S from LABOCA on APEX (Weiβ et al. 2009), the combined AzTEC+MAMBO 1.1 mm map of GOODS-N (Penner et al. 2011), and MAMBO 1.2 mm imaging of xFLS (Lutz et al. 2005; Sajina et al. 2008; Martínez-Sansigre et al. 2009), which exists for 169 galaxies. For four of these, the source redshift is high enough that there is no data beyond \( \lambda = 250 \, \mu \)m, which is our threshold for calculating dust mass. We also remove any sources from the sample where the submillimeter emission is blended with a nearby source (10 sources). We remove 57 galaxies for hosting an AGN. Finally, we remove 47 galaxies for having submillimeter photometry with \( S/N < 2 \), leaving a final sample of 51 galaxies.

### 2.4. Selection Effects

We are comparing the far-IR/submillimeter properties of three different samples with different selection criteria, so we must understand whether our results are biased due to the selection criteria. The GOALS sample is selected at 60 \( \mu \)m while the 5MUSES sample and the Supersample are selected at observed frame 24 \( \mu \)m; this selection criteria alone could produce samples of galaxies that are warmer or colder for the same \( L_{\text{IR}} \) range.

We consider the 5MUSES and GOALS sources together to make up our low-\( z \) sample. All of the 5MUSES sources with \( L_{\text{IR}} > 10^{11} \) (same as GOALS) would be selected at rest frame \( S_{24} > 5.24 \) Jy, the GOALS selection criterion. Similarly, all GOALS galaxies meet the 5MUSES selection criterion of \( S_{24} > 5 \) mJy.

We use the mid-IR spectrum to determine if a 5MUSES source meets the Supersample selection criterion, since at \( z = 1–2 \), \( S_{24} \) covers the PAH features. Only 28% of the 5MUSES sample would be selected at \( z = 1 \), and 11% at \( z = 2 \). This is not surprising, since the 5MUSES galaxies are on average less luminous. Only 32% of the 5MUSES galaxies overlap in the \( L_{\text{IR}} \) range spanned by the Supersample. However, of the 60 5MUSES galaxies with \( L_{\text{IR}} > 2 \times 10^{11} L_\odot \) (the same range as the bulk of the Supersample), 50 would be selected as Supersample galaxies at \( z = 1 \) and 30 would be selected at \( z = 2 \), due to \( L_{\text{PAH}}/L_{\text{IR}} \) ratios similar to \( z \sim 1–2 \) (U)LIRGs (Pope et al. 2013; Kirkpatrick et al. 2014b; Battistit et al. 2015).

Estimating whether the GOALS sources would be included in our Supersample is more nuanced, since we lack global IRS spectra for the GOALS galaxies. Instead, we use the Chary & Elbaz (2001) library of templates, which were derived from the IRAS BGS. At \( z = 1 \), templates with log \( L_{\text{IR}} > 11.11 L_\odot \) meet the selection threshold, but at \( z = 2 \), this increases to log \( L_{\text{IR}} > 12.21 L_\odot \).

Next, we estimate what fraction of the Supersample would be selected as a 5MUSES or GOALS galaxy, if the Supersample existed at a different redshift. This is largely an academic exercise, since the Supersample contains the most luminous galaxies, and Symeonidis et al. (2011) demonstrated that the IRAS selection criteria are sensitive to ULIRGs (\( L_{\text{IR}} > 10^{12} L_\odot \)) with \( T = 17–87 \) K. Nevertheless, such a check will ensure that the Supersample contains enough warm dust to be luminous at rest-frame 60 and 24 \( \mu \)m. We calculate synthetic 60 \( \mu \)m photometry following the prescription in Section 3.2, for a redshift of \( z = 0.015 \), which is the peak of the GOALS redshift distribution in Figure 1. Ninety-seven percent of the Supersample meets the GOALS selection criterion. The 5MUSES selection criterion is \( S_{24} > 5 \) mJy. We shift our synthetic rest-frame photometry to \( z = 0.15 \) by scaling down by 1.62, a ratio determined using the Kirkpatrick et al. (2013b) template library. Again, 97% would be selected as a 5MUSES galaxy.

From this, we conclude that if cold, massive galaxies, like most of the Supersample, exist at lower redshift, they are easily detectable in current surveys. Similarly, at \( z \sim 1 \) at least, we should be able to select a population of galaxies with the range of dust masses and temperatures exhibited by local LIRGs, if they exist. However, at \( z \sim 2 \), galaxies with spectral shapes similar to local LIRGs are undetectable in current 24 \( \mu \)m surveys.

### 2.5. ULIRG Nomenclature

Throughout the remainder of this paper, we dispense with the (U)LIRG nomenclature for clarity. In the local universe, the term ULIRG evokes a massive merging system, where the merger gives rise to a starburst followed by an AGN (Sanders & Mirabel 1996). At earlier times, the correlation between ULIRGs and mergers still exists, but is more tenuous, and the link between mergers and starbursts is even less clear in these systems (Hopkins et al. 2010; Kartaltepe et al. 2012; Hayward et al. 2013). LIRGs and ULIRGs are simply luminosity cuts, so to avoid any preconceived notions between these luminosity cuts and physical properties, we follow the convention in Casey et al. (2014) and refer to objects in all three samples as DSFGs.

### 3. Data and Physical Properties

In this paper, we compare three samples of IR luminous galaxies at three different epochs. For a fair comparison, we shift all IR photometry to the rest frame, we remove any AGN contribution using Spitzer spectroscopy, and we derive dust masses self-consistently. By using the mid-IR spectrum to look for a hot dust continuum, which we attribute to an AGN, we are also removing galaxies with a hot central starburst.

#### 3.1. Identifying and Removing AGNs

The mid-IR spectrum (\( \lambda = 3–20 \, \mu \)m) is rich for identifying star formation features and AGNs. The most prominent dust emission complexes are produced by PAHs (\( \lambda = 6.2, 7.7, 11.3, 12.7 \, \mu \)m), which are abundant in galaxies with metallicity close to solar, such as high-redshift DSFGs (Magdis et al. 2012). These molecules are preferentially located in the photodissociation regions surrounding star-forming regions (Helou et al. 2005). As such, PAHs are good tracers of ongoing star formation in a galaxy (Peeters et al. 2004). However, the mid-IR spectrum can also exhibit continuum emission due to the torus enveloping the AGN.

We perform spectral decomposition of the mid-IR spectrum (\~5–15 \( \mu \)m rest frame) for each source in all three samples in order to disentangle the AGN and star-forming components. Pope et al. (2008) explain the technique in detail, and we summarize it here. We fit the individual spectra with a model comprising four components: (1) the star formation component is represented by the mid-IR spectrum of the prototypical starburst M82, (2) the AGN component is determined by fitting a pure power law (\( \lambda^\alpha \)) with the slope and normalization (\( N \)) as free parameters, (3, 4) extinction curves from the Weingartner & Draine (2001) dust models for Milky Way (MW) type dust is applied to the AGN component and star-forming component.
The full model is then
\[
S_\nu = N_{\text{AGN}} \nu^\alpha e^{-\tau_{\text{AGN}}} + N_{\text{SF}} S_\nu(M82)e^{-\tau_{\text{SF}}}. \tag{1}
\]
We fit for \(N_{\text{AGN}}, N_{\text{SF}}, \alpha, \tau_{\text{AGN}},\) and \(\tau_{\text{SF}}\) simultaneously.

For each source, we quantify the strength of the AGN, \(f(\text{AGN})_{\text{MIR}},\) as the fraction of the total mid-IR luminosity (\(\lambda = 5-15\ \mu\text{m}\)) coming from the power-law continuum component. For the GOALS sample, our AGN identification technique selects the same sources as the \(S_{25}/S_{5}\) versus \(S_{6.7}/S_{5}\) diagnostic applied in Petric et al. (2011). For the 5MUSES sources, we also identify the same AGNs as Wu et al. (2010), where the authors classify AGNs on the basis of the 6.2 \(\mu\text{m}\) PAH feature equivalent width alone.

In Kirkpatrick et al. (2013b), we found that an AGN had a significant contribution to the far-IR emission, quantified through dust temperatures and luminosities, when \(f(\text{AGN})_{\text{MIR}} \gtrsim 0.5.\) Recently, Lee et al. (2016) showed that local dust-obscured galaxies hosting an AGN had lower dust masses than their star-forming counterparts. Consequently, we remove all 5MUSES, GOALS, and Supersample galaxies with \(f(\text{AGN})_{\text{MIR}} \geq 0.5,\) so that we are only comparing the far-IR/submillimeter properties of strongly star-forming systems. We note that because the GOALS sample is nearby, in some cases IRS observations only cover the central region of the galaxy, in contrast to the IRS observations of 5MUSES and the high-z Supersample. This could introduce a slight bias as we may remove sources that have a nucleus dominated by AGN emission, whereas the galaxy-integrated emission is dominated by star formation. We only remove 13% of the GOALS sample, so the effects of this potential bias are small.

Our AGN identification technique only relies on detecting hot continuum emission in the mid-IR. While we attribute this to an AGN, in principle, a very compact, dust-enshrouded starburst would display the same mid-IR signature. By removing AGNs, we are also then removing these compact starbursts, which will have different ISM properties than galaxies where the star-forming regions are located throughout the galaxy, due to higher gas densities and a harsher radiation field. However, we note that although such compact starbursts exist locally (e.g., Díaz-Santos et al. 2010b), so far such galaxies are rare at high redshift and still have prominent PAH features (Nelson et al. 2014). From the Supersample, we remove 47% for having \(f(\text{AGN})_{\text{MIR}} \geq 0.5,\) and 62% of these removed sources have X-ray detections consistent with being an AGN (Kirkpatrick et al. 2013b), while the remaining sources may be Compton thick based on predicted X-ray luminosities (Kirkpatrick et al. 2012). As such, we do not think that we are missing a large population of compact starbursts by removing sources with \(f(\text{AGN})_{\text{MIR}} \geq 0.5.\)

### 3.2. Calculating Rest-frame Photometry

In Section 4, we compare the far-IR SED shape of GOALS, 5MUSES, and the Supersample by utilizing far-IR colors. To make a fair comparison between three samples at different redshift ranges, we require synthetic rest-frame photometry in the MIPS and SPIRE photometric bandpasses for 5MUSES and the Supersample. GOALS is at low enough redshift that the offset in rest-frame wavelengths is negligible. We fit templates to the Supersample and 5MUSES from the MIR-based library in Kirkpatrick et al. (2013b). The MIR-based library is a suite of 11 empirical templates that characterize the full shape of the IR SED based on the relative amounts of PAH and continuum emission in a source’s mid-IR spectroscopy. We select the appropriate template for each source from the spectral decomposition described above, fit to the far-IR photometry (\(\lambda > 20\ \mu\text{m}\)), and then convolve each template with the MIPS and SPIRE transmission filters to create synthetic rest-frame photometry at 70, 160, and 250 \(\mu\text{m}\). We plot the Supersample intrinsic SEDs and estimated rest-frame photometry in Appendix A. The biggest concern when interpolating between data points is whether we have chosen a template with the correct far-IR shape. However, the majority of galaxies have a sufficiently well-sampled far-IR SED to mitigate this uncertainty, as the estimated photometry lies very close to the observed data points.

It is unlikely that an AGN that is not significantly affecting the mid-IR emission would have a strong effect on the far-IR emission. Even so, we correct the rest-frame broadband colors and \(L_{\text{IRs}}\) of all SFGs with \(0.0 < f(\text{AGN})_{\text{MIR}} < 0.5\) in order to account for any scatter introduced by a buried AGN that may contribute to, but not dominate, the IR luminosity. We have calculated these corrections by decomposing empirical templates into their relative star formation and AGN components as described in detail in Kirkpatrick et al. (2013b). The AGN corrections are listed below, for the rest-frame luminosities. In Kirkpatrick et al. (2013b), we discuss ways to estimate \(f(\text{AGN})_{\text{MIR}}\) in the absence of mid-IR spectroscopy, so these corrections can be applied to sources with only broadband photometry:

\[
\begin{align*}
L_{\text{IR}}^\text{SF} &= L_{\text{IR}} \times (1 + 0.035f(\text{AGN})_{\text{MIR}} - 0.66f(\text{AGN})_\text{MIR}^2) \\
L_{160}^\text{SF} &= L_{160} \times (1 - 1.81f(\text{AGN})_{\text{MIR}} + 0.94f(\text{AGN})_\text{MIR}^2) \\
L_{24}^\text{SF} &= L_{24} \times (1 - 0.08f(\text{AGN})_{\text{MIR}} - 0.16f(\text{AGN})_\text{MIR}^2) \\
L_{70}^\text{SF} &= L_{70} \times (1 - 0.036f(\text{AGN})_{\text{MIR}}) \\
L_{250}^\text{SF} &= L_{250} \times (1 - 0.018f(\text{AGN})_{\text{MIR}}).
\end{align*}
\tag{2}
\]

#### 3.3. Dust Mass

With our three samples, we can compare how \(M_{\text{dust}}\) evolves in dusty galaxy populations with redshift. Dust mass is calculated as

\[
M_{\text{dust}} = \frac{S_\nu D_L^2}{\kappa_\nu B_\nu(T)},
\tag{3}
\]

where \(B_\nu(T)\) is the Planck equation, \(\kappa_\nu\) is the dust opacity, \(D_L\) is the luminosity distance, and \(S_\nu\) is the flux density. For \(S_\nu,\) we use the longest far-IR/submillimeter data available, which varies with each sample. We only use sources whose rest-frame measurement is \(\lambda \geq 250\ \mu\text{m},\) otherwise the dust emission may not be tracing the coldest dust component (Scoville et al. 2016). When we combine this criterion with the \(f(\text{AGN})_{\text{MIR}} < 0.5\) criterion, we have the final sample sizes of 46 galaxies from GOALS, 30 galaxies from 5MUSES, and 52 galaxies from the Supersample.

We take \(\kappa_\nu,\) the dust opacity, from the Weingartner & Draine (2001)\(^{17}\) models at the rest wavelength of \(S_\nu\) for each individual source. We assume MW-like dust and \(R_V = 3.1,\) although in

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\(^{17}\) Recent results indicate a change in these model opacities (Dalcanton et al. 2015; Planck Collaboration 2016), but we are consistently using the same model for every source, so we do not expect any change in opacity to affect our dust mass comparison.
these models, the far-IR/submillimeter opacities have negligible changes for different $R_V$ and are similar for the MW-, LMC-, and SMC-type models (at 850 $\mu$m, the opacity differs by $<10\%$).

Scoville et al. (2016) argue for using fixed $T_{\text{cold}}$, since presumably the temperature in the diffuse ISM should be relatively similar for all massive, dusty galaxies, assuming similar radiation fields and dust grain mixtures. Indeed, in Kirkpatrick et al. (2013b) we found that the average cold dust temperature in SFGs in the Supersample was remarkably constant, $T \approx 26$ K, and did not scale with $L_{\text{IR}}$. Accordingly, we set $T_{\text{cold}} = 25$ K for all three samples and derive $M_{\text{dust}}$ using Equation (3). As a test of this assumption, we fit each galaxy with a two-temperature modified blackbody with $T_{\text{cold}} = 25$ K and achieve excellent fits for all sources. We explore how the dust masses change if $T_{\text{cold}}$ is allowed to vary in Appendix B and find that all conclusions in this paper hold regardless of the specific method of measuring dust mass as long as these measurements are consistent across all three samples. In this study, we are primarily concerned with comparing the dust masses change if the other dust and achieve excellent changes for different $\beta$. We use the $L_{\text{IR}}$ compiled from the literature for each sample (see Section 2). In all cases, the $L_{\text{IR}}$ was not determined using the submillimeter data that goes into the $M_{\text{dust}}$ calculation, so in this way, $L_{\text{IR}}$ and dust mass are independent. $L_{\text{IR}}$ for the 5MUSES and Supersample galaxies were measured by fitting template libraries, so the main source of concern is how the choice of $\beta$ used in constructing the templates might affect $L_{\text{IR}}$, as $M_{\text{dust}}$ also depends on $\beta$. We calculate that varying $\beta \in [1.5, 2.0]$ changes $L_{\text{IR}}$ by 5%, so using different values of $\beta$ to calculate $L_{\text{IR}}$ and $M_{\text{dust}}$ will not be a significant source of scatter in the resulting relationships. In the analysis below, we correct $L_{\text{IR}}$ for any contribution from nuclear activity as indicated by the presence of a hot dust continuum in the mid-IR spectrum, so that we are actually comparing $M_{\text{dust}}$ with $L_{\text{IR}}$. The correction is at most 0.07 dex. As all of the GOALS and 5MUSES photometry and redshifts used in this paper are published elsewhere in the literature (Wu et al. 2010; U et al. 2012; Magdis et al. 2013), we only list the $M_{\text{dust}}$ and $L_{\text{IR}}$ values that we have calculated for the Supersample in Table 1.

3.4. Stellar Mass

Stellar masses are compiled from the literature. For GOALS, U et al. (2012) calculates $M_*$ by fitting Bruzual & Charlot (2003) stellar population models to 10 different broadband UV-NIR photometry points (from GALEX, ground-based observatories, and Spitzer). The star formation history is parameterized as SFH = $e^{-t/\tau}$ with $\tau \in [1, 30]$ Gyr. Metallicity is a free parameter. The authors choose a Chabrier initial mass function (IMF; Chabrier 2003) with a mass range of $0.1 M_\odot$–$100 M_\odot$.

Shi et al. (2011) calculate stellar masses for the 5MUSES sample by fitting Bruzual & Charlot (2003) stellar population models to UV-IR data assuming a Chabrier IMF. The SFH has $\tau \in [0.03, 22.4]$ Gyr, and metallicity is a free parameter.

For the GOODS and ECFDS sources (we do not have $M_*$ for the six xFLS sources included in the final high-$z$ sample), Kirkpatrick et al. (2012) describes the procedure for calculating $M_*$ by fitting Bruzual & Charlot (2003) models to a suite of photometry from the $U$ band to 4.5 $\mu$m (see also Pannella et al. 2015). For the SFH, $\tau \in [0.1, 20]$ Gyr and metallicity is fixed to solar. For the Supersample, a Salpeter IMF is used (Salpeter 1955), which results in higher stellar masses than a Chabrier IMF. We convert the Supersample masses to a Chabrier framework using $M_{\text{Chab}} = 0.62 M_{\text{Sal}}$ (Zahid et al. 2012; Speagle et al. 2014).

We are drawing from three different samples fit with three different methods, so we verify the stellar masses by comparing with the rest-frame $K$-band estimated $M_*$ (Howell et al. 2010). In all cases, the stellar masses are consistent to within 0.6 dex, which is the largest deviation. We further check the consistency of the Supersample masses, since these were initially calculated with a Salpeter IMF and require a conversion. We fit the UV-submillimeter SEDs of 10 randomly selected galaxies with the MAGPHYS code, which employs an energy-balance technique to simultaneously fit the UV/optical/IR emission (da Cunha et al. 2008). The MAGPHYS-derived stellar masses are on average 0.2 dex larger than the masses from Kirkpatrick et al. (2012), converted to a Chabrier IMF.

All three samples cover a similar range of $M_* = 1 \times 10^{8.5}$–$3 \times 10^{11} M_\odot$, as can be seen in Figure 8.

4. SED Comparison

We look for evolution in the IR SED of our samples of DSFGs by comparing rest-frame colors, as this does not require any model assumptions. We show a sample SED at $z \sim 1$ and the MIPS and SPIRE 250 $\mu$m broadband photometry filters in Figure 2 as a visual guide when comparing galaxy colors below. We also plot a local template from the Chary & Elbaz (2001) library to better illustrate how the far-IR colors can indicate SED shape. We plot a local template that peaks at the same wavelength as our $z \sim 1$ template, despite being nearly an order of magnitude lower in luminosity, so that the color $L_{250}/L_{70}$ should be approximately equal for both the local and $z \sim 1$ templates. However, the $z \sim 1$ template has proportionally more cold dust, as evidenced by an increase in the emission longwards of ~200 $\mu$m.

In Figure 3, we compare $L_{160}/L_{70}$ and $L_{250}/L_{70}$. The peak of the SED is traced by $L_{160}/L_{70}$, which is also a proxy for $T_{\text{dust}}$. $L_{250}/L_{70}$ is difficult to interpret decoupled from $L_{160}/L_{70}$ SF. If $L_{250}/L_{70}$ indicates temperature, then for a given $T_{\text{dust}}$, $L_{250}/L_{70}$ can be thought of as the amount of cold dust (traced by $L_{250}/L_{70}$ relative to warm dust (traced by $L_{70}$)). SEDs with proportionally more warm dust will have smaller ratios of $L_{250}/L_{70}$. All three samples have a tight relationship between $L_{160}/L_{70}$ and $L_{250}/L_{70}$. Physically, this relationship can be described by how the incident radiation field in the ISM drives the far-IR emission (Witt & Gordon 2000; Miseault et al. 2001; Dale & Helou 2002; Dale et al. 2014), which we illustrate using the suite of IR star-forming templates from Dale et al. (2014). These model SEDs are created by combining the emission from different dust mass elements, heated by an incident radiation field of strength $U$, in a power-law distribution:

$$dM_{\text{dust}} \propto U^{-\alpha}dU.$$ (4)

We chose the Dale et al. (2014) templates due to the simplicity of interpretation. In this formulation, $\alpha$ characterizes the relative contributions of each dust mass element to the total...
Sed, so that a smaller \( \alpha \) means more of the dust in a galaxy is heated by a harsher radiation field. We show the location of the Dale et al. (2014) templates in Figure 3 using the thick grayscale line. Our sources cluster around this line and have colors suggestive of \( \alpha \in [1.125, 3.375] \), with the low-\( z \) (GOALS + 5MUSES) and high-\( z \) samples spanning a similar range of \( \alpha \).

The two low-redshift samples show a distinct offset along the dark line, which is not unexpected given the different luminosities probed by 5MUSES and GOALS. We measure
Figure 2. We illustrate where the broadband MIPS 24, 70, and 160 μm and SPIRE 250 μm transmission filters sample the SED using a representative SFG template (red line) at z = 1 (Kirkpatrick et al. 2012) with log $L_{\text{IR}} = 11.62 L_\odot$. To illustrate how the far-IR SED changes, we also plot a template (green dashed line) from the local Chary & Elbaz (2001) library, with log $L_{\text{IR}} = 10.79 L_\odot$. The templates have been arbitrarily normalized so that the peaks coincide. The $z \sim 1$ template has proportionally more cold dust, notably at 250 μm, than the local template.

4.1. Trends with $L_{\text{IR}}^{\text{SF}}$

Our higher-$z$ sample is also at a higher $L_{\text{IR}}$, which can confuse any redshift evolution. We compare $L_{160}^{\text{SF}}/L_{70}^{\text{SF}}$ with $L_{250}^{\text{SF}}/L_{70}^{\text{SF}}$ in Figure 4. Figure 4 shows a clear trend between $L_{160}^{\text{SF}}/L_{70}^{\text{SF}}$ and $L_{250}^{\text{SF}}/L_{70}^{\text{SF}}$, otherwise known as the $L_{\text{IR}}^{\text{SF}}$-T$_{\text{dust}}$ relation (Chapman et al. 2003; Casey et al. 2012; Magnelli et al. 2014; Lee et al. 2016). We overplot the mean of each sample in log($L_{\text{IR}}^{\text{SF}}$) bins of 0.25 as the larger symbols. The 5MUSES and GOALS galaxies follow the same general trend, but there is a clear offset between the low-$z$ samples and Supersample, due to evolution of the $L_{\text{IR}}$-T$_{\text{dust}}$ relationship with redshift (Chaplin et al. 2009; Casey et al. 2012; Magnelli et al. 2014). At a given $L_{\text{IR}}^{\text{SF}}$, the difference between low $z$ and high $z$ is ~0.2 dex, which corresponds to approximately a 5 K temperature difference. The Supersample galaxies have a much larger scatter than the GOALS sample, illustrating the increasing diversity of DSFGs with redshift (Symeonidis et al. 2011). Interestingly, the 5MUSES galaxies with log $L_{\text{IR}}^{\text{SF}} > 11.4$ overlap with the Supersample rather than the GOALS sample. These are also the highest redshift 5MUSES galaxies, with $z > 0.15$, and they also overlap with the Supersample below in Figure 5. Overall, we see a similar slope in the mean $L_{160}^{\text{SF}}/L_{70}^{\text{SF}}$ versus $L_{250}^{\text{SF}}$ points, with a normalization that depends on redshift, in agreement with the findings in Magnelli et al. (2014) and Casey et al. (2012).

5. Evolving Trends with Dust Mass

We now consider the physical parameter, $M_{\text{dust}}$. We have calculated $M_{\text{dust}}$ in a self-consistent manner for all galaxies, while making as few assumptions as possible. Figure 5 shows a clear, strong trend between $M_{\text{dust}}$ and $L_{\text{IR}}^{\text{SF}}$ (Kendall’s $\tau = 0.68$). The dashed line is fit to the 5MUSES and GOALS galaxies, and almost all the Supersample sources lie above this relation. The fit is sublinear, with

$$M_{\text{dust}} = 2.26 \times (L_{\text{IR}}^{\text{SF}})^{0.653}.$$  

For clarity, the error bars on each point only reflect the error of the submillimeter flux used to calculate $M_{\text{dust}}$. The effect of changing $T_{\text{cold}}$ by ±5 K is illustrated by the solid bar in the bottom-right corner of Figure 5 (M. Han et al. 2017, in preparation). At first approximation, one might expect that
$L_{\text{IR}} / M_{\text{dust}} \propto T_{\text{dust}}^{-4+\beta}$ in the optically thin regime, if the dust emission can be represented with a single-temperature modified blackbody (Lanz et al. 2014; Magnelli et al. 2014). This simplification would imply a linear relationship between $L_{\text{IR}}$ and $M_{\text{dust}}$ for a fixed $T_{\text{dust}}$. Since we measure a sublinear trend, this means that this model is unphysical since dust has a range of temperatures, and other effects, such as optical depth or geometry, are affecting the far-IR/submillimeter emission.

Although in the top panel of Figure 5 it appears that all samples may actually lie along the same relationship between $L_{\text{IR}}$ and $M_{\text{dust}}$, two separate relationships become evident in the bottom panel of Figure 5, where we show $L_{\text{IR}} / M_{\text{dust}}$ versus $\frac{H}{\text{ins}}$. There is a strong trend between $L_{\text{IR}} / M_{\text{dust}}$ and $L_{\text{IR}}$ with more luminous galaxies having proportionally less dust for a given radiation field, which results in warmer temperatures (Kendall’s $\tau = 0.49$ (0.67) for the low (high) $z$ samples). However, this trend (plotted as the solid line) shifts with redshift, so that the Supersample galaxies with $L_{\text{IR}} = 10^{12} L_{\odot}$ have $L_{\text{IR}} / M_{\text{dust}}$ ratios similar to GOALS galaxies with $L_{\text{IR}} = 2 \times 10^{11} L_{\odot}$ (shown by the dotted line); a complementary result was found for submillimeter galaxies in Chakrabarti & McKee (2008). The 5MUSES galaxies have a flatter distribution, although the galaxies that clearly overlap the Supersample are the galaxies at higher redshifts ($z > 0.15$).

Similarly, Magdis et al. (2014) found that intermediate-redshift DSFGs had larger gas reservoirs and lower dust temperatures than their local counterparts by a redshift of $z \sim 0.33$.

Submillimeter fluxes can also be used to calculate gas mass (Scoville et al. 2016), although this requires extra assumptions, such as the expected dust-to-gas ratio. We illustrate on the right axis in Figure 5 what the $H_2$ gas mass would be, following the formalism of Scoville et al. (2016):

$$M_{H_2} = c_{850} L_{850},$$

where $c_{850} = 6.7 \times 10^{19} \text{erg s}^{-1} \text{Hz}^{-1} \text{M}_\odot^{-1}$. We have CO luminosities for a handful of 5MUSES and Supersample galaxies (Yan et al. 2010; Kirkpatrick et al. 2014b), and $M_{H_2}$ calculated from $L_{\text{CO}}$ for these galaxies agrees with the $M_{H_2}$ calculated from $L_{850}$. Furthermore, the gas masses we derive here for our high-$z$ sample are completely consistent with the gas masses in Scoville et al. (2016) for galaxies spanning the same $L_{\text{IR}}$ and redshift ranges. We then convert $L_{\text{SF}}^{\text{IR}}$ to SFR with SFR [$M_\odot \text{yr}^{-1}] = 1.59 \times 10^{-10} \times L_{\text{SF}}^{\text{IR}} [L_{\odot}]$ from Murphy et al. (2011). In the bottom panel, we show how $L_{\text{SF}}^{\text{IR}} / M_{\text{dust}}$ translates to SFR/$M_{H_2}$, which is the star formation efficiency (SFE). The relationship between SFE and $L_{\text{SF}}^{\text{IR}}$ evolves with redshift. That is, at a given $L_{\text{SF}}^{\text{IR}}$, local galaxies convert gas to stars more efficiently than high-$z$ galaxies. Assuming a dust-to-gas ratio of ~100, the $L_{\text{SF}}^{\text{IR}} / M_{\text{dust}}$ relation for the Supersample is in excellent agreement with that predicted by hydrodynamical simulations combined with radiative transfer (Figure 9 of Hayward et al. 2012). We remind the reader that we are comparing galaxies at a fixed luminosity, rather than at a fixed location on the main sequence, which we examine in Section 6.3. At $L_{\text{SF}}^{\text{IR}} > 10^{11}$, local DSFGs lie predominantly above the main sequence, while $z \sim 1$–2 DSFGs lie on it, which would account for the difference in SFEs.

We now return to the question of what drives the cooler dust temperatures observed in higher-redshift galaxies. Based on simulations, Safarzadeh et al. (2016) predict that $L_{\text{IR}}$ and $M_{\text{dust}}$ alone determine the shape of the SED, independent of the size of the galaxy. That is, $T_{\text{dust}}$ depends solely on the total luminosity absorbed by dust ($L_{\text{IR}}$) and the amount of absorbing material ($M_{\text{dust}}$), in which case it is not necessary to measure all three parameters for a galaxy, since the third parameter can be inferred from the other two. We test this prediction with observations in Figure 6, where we plot $L_{\text{SF}}^{\text{IR}} / M_{\text{dust}}$ versus $L_{\text{IR}} / L_{\odot}$, a proxy for $T_{\text{dust}}$.

There is a clear correlation between the parameters (Kendall’s $\tau = -0.51$), and crucially, there is no offset with redshift. Magdis et al. (2012) found that $L_{\text{IR}} / M_{\text{dust}}$ is proportional to $(U)$, the average interstellar radiation field. In turn, $(U)$ determines $T_{\text{dust}}$, giving rise to the strong correlation (Draine & Li 2007). The dotted–dashed line shows the relationship

$$\log \left( \frac{L_{\text{IR}}^{\text{SF}}}{M_{\text{dust}}} \right) = -1.24 \times \log \left( \frac{L_{\text{IR}}^{\text{SF}}}{L_{70}^{\text{SF}}} \right) + 3.68,$$

which we have derived using all three samples, so this parameterization holds over three orders of magnitude ($L_{\text{IR}}^{\text{SF}} = 10^{10}$–$10^{13} L_{\odot}$) and from $z \sim 0$–2. This parameterization can be used to estimate $M_{\text{dust}}$ from far-IR data without requiring a longer wavelength ($\lambda > 500 \mu\text{m}$) observation. This relationship is also observed on much smaller scales (≤1 kpc) in local resolved galaxies from the KINGFISH survey (Kirkpatrick et al. 2014a). We calculate the residuals around the best-fit line and show these in the bottom panel of Figure 6. Although the Supersample galaxies have a mean residual of $-0.14$ dex, indicating they lie slightly below the best-fit line,
the scatter of the residuals is quite large (standard deviation of 0.28 dex). Combined with the large uncertainties on the dust masses, this argues against any strong redshift evolution in Equation (7).

With the data available to us, the source of scatter in this figure is open to interpretation. One likely source is the geometry of the ISM, which can explain how galaxies with the same L_{IR}/M_{dust} can have different L_{SF}/L_{70} ratios. A galaxy whose ISM approximates a shell geometry, where the stars are enclosed within the shell, will always peak at shorter wavelengths than an ISM geometry where the stars and dust are well mixed, all other parameters being equal (Misselt et al. 2001). This is because the shell geometry absorbs all of the incident radiation from stars, heating the dust to higher temperatures. Testing whether different geometries can account for all of the scatter between L_{IR}/M_{dust} and L_{160}/L_{70} will require resolved observations of the ISMs with ALMA.

The relationship between L_{IR}/M_{dust} and L_{160}/L_{70} can also explain the offset between the low- and high-z samples in Figure 4. It is possible that the normalization of the L_{IR}–T_{dust} relation evolves with redshift because galaxies at z = 1–2 have higher dust masses at a given L_{IR} (Magdis et al. 2012). If at fixed L_{IR}, the typical dust mass is higher in high-redshift DSFGs than in their z ~ 0 counterparts, then the dust temperature will be lower, shifting the normalization of the L_{IR}–T_{dust} relation (Safarzadeh et al. 2016). This explanation for the shift does not require any change in the mode of star formation or ISM density (compact starburst versus main sequence) or possibly in the dust composition. To produce colder temperatures for a given radiation field, an increase in the amount of large dust grains, relative to small ones, is required if the far-IR emission is optically thin. However, in the ULIRG regime, the high dust masses can cause the dust to be optically thick even at submillimeter wavelengths (e.g., González-Alfonso et al. 2004), in which case simply adding more dust (and not changing the proportion of large to small grains) will decrease the temperature.

6. Discussion

6.1. Potential Evolution in Dust Properties?

The DSFGs at z ~ 1–2 have higher dust masses for a given L_{SF} than local DSFGs. Here, we want to make an important distinction. The observed quantity in our sample is the luminosity density in the Rayleigh–Jeans tail, and it is the luminosity density that is actually higher in high-redshift galaxies (as we have used the same assumptions for all other parameters when calculating M_{dust}). The luminosity density in the Rayleigh–Jeans tail is directly proportional to M_{dust} × κ_v, meaning that in principle, M_{dust} and κ_v are degenerate. Thus far, we have been assuming the same opacity relationship for all galaxies, but in reality, the opacity might be evolving with redshift rather than the M_{dust}. Dust opacity has a wavelength dependence

$$\kappa_\nu = \kappa_0 \left( \frac{\lambda}{\lambda_0} \right)^{-\beta},$$

so that either the normalization, κ_0, or the slope, β, could be evolving.

Although the Weingartner & Draine (2001) models all have similar κ_v values in the submillimeter, grain compositions and distributions that differ considerably from these models can give different submillimeter opacities. The apparent increase in dust mass could possibly be due to a change in the dust grain properties with redshift (Dwek et al. 2014). For example, ice mantles can affect β, causing opacity to increase, and ice mantles should be prevalent in cold star-forming regions (Tielens et al. 1984; Bergin et al. 2000; Spoon et al. 2002). The presence of ice mantles can increase κ_v by a factor of four (Preibisch et al. 1993; Pollack et al. 1994) a factor of four increase in κ_v for the high-redshift galaxies would reconcile the difference in M_{dust} for GOALS and the Supersample. The strength of water ice, silicate absorption, and 3.4 μm PAH emission features has been measured in a handful of Supersample sources and closely resembles what is measured in local GOALS galaxies with similar obscuration, providing some indication that the amount of ice in dusty galaxies does not strongly evolve with redshift (Sajina et al. 2009).

If β in our galaxies differs significantly from β in the Weingartner & Draine (2001) models, for example, varying with redshift, then our assumed κ_v will be incorrect. The emissivity measure from the Rayleigh–Jeans tail is observed to be shallower in lower metallicity galaxies (Galametz et al. 2011; Kirkpatrick et al. 2013a), though there is little evidence that metallicity evolves strongly in massive, dusty galaxies out to z ~ 2 with similar M_{dust}, SFR, and M_{med} (Mannucci et al. 2010; Magdis et al. 2012; Bothwell et al. 2016). In fact, when we measure β directly for individual galaxies by fitting a modified blackbody with T = 25 K, we find β = 1.8 for the Supersample and β = 2.02 for the GOALS sample. We are not fully sampling the Rayleigh–Jeans tail in the Supersample, and longer wavelength observations are required to more accurately measure the effective β. However, with current observations,
we see little evidence supporting a drastic increase in opacity to reconcile the dust mass measurements of our samples. Longer wavelength observations, such as with ALMA or the Large Millimeter Telescope, are required to better measure the effective $\beta$ at $z = 1$–2.

6.2. Potential Role of Mergers or Compactness?

Additional insight into the ISM of galaxies can be gained by examining morphologies and merger signatures, which we have for the GOALS and Supersample sources. Galaxies hosting a compact central starburst will have a higher temperature than galaxies at the same $L_{\text{IR}}$, which are disks (Chanial et al. 2007). In local LIRGs and ULIRGs, a compact starburst is triggered by a major merger, as the transfer of angular momentum funnels gas to the central kiloparsec of the merging system.

Stierwalt et al. (2013) classified the GOALS sample into merger classifications using $HST B$-, $I$-, and $H$- band imaging (see also Haan et al. 2011) and IRAC 3.6 $\mu$m imaging. All 46 galaxies in the present work also have a merger classification. The merger classifications we use here are: 0: no merger or massive neighbor; 1: galaxy pair; 2: early-stage (disk still intact); 3: mid-stage (amorphous disk, tidal tails); and 4: late-stage (two nuclei in common envelope). Morphology analysis of the Supersample is less straightforward due to our combining different surveys. GOODS-S and GOODS-N galaxies have been visually classified with $HST$ WFC3 images as part of the Cosmic Assembly Near-IR Deep Extragalactic Legacy Survey (CANDELS; P. I. S. Faber & H. Ferguson). The CANDELS tool gives classifiers a choice of five different interaction stages, similar to those listed above. The morphology catalogs then contain the fraction of classifiers that selected each interaction stage (Kartaltepe et al. 2015). We use these fractions to determine a weighted average interaction stage, from 0 to 4 (see also Rosario et al. 2015, who create a weighted average on a 0–1 scale). Zamojski et al. (2011) classifies 134 XFLS sources into merger classifications using $Hubble$ NICMOS imaging, from 0 to 5. Here, we combine old mergers (5) with advanced mergers (4), to match the categories described above. In total, 17 Supersample galaxies have dust masses and a merger classification. 5MUSES galaxies lack a morphology classification.

The top panel of Figure 7 shows the interaction stage as a function of $L_{\text{IR}}^{\text{SF}} / M_{\text{dust}}$, and the points are shaded by $L_{160}^{\text{SF}} / L_{70}^{\text{SF}}$. There is no correlation between the parameters, for either GOALS or the Supersample. Galaxies at a given $L_{\text{IR}}^{\text{SF}} / M_{\text{dust}}$ occupy all merger classifications, as do galaxies at a given $L_{160}^{\text{SF}} / L_{70}^{\text{SF}}$. DSFGs exhibit a variety of $L_{\text{IR}}^{\text{SF}} / M_{\text{dust}}$ ratios and a variety of major merger classifications, indicating that the major merger scenario cannot directly explain all of the far-IR observed properties of these galaxies. In the same vein, using hydrodynamical simulations post-processed with dust radiative transfer, Lanz et al. (2014) found that the effective dust temperature of mergers does not reflect the merger stage except for a very short period ($\lesssim 100$ Myr) during the coalescence-induced starburst.

The most direct test of how ISM geometry affects $L_{\text{IR}}^{\text{SF}} / M_{\text{dust}}$ and $T_{\text{dust}}$ is to compare the spatial extent of the dusty ISM. Measuring millimeter sizes on a resolved scale at low and high redshift requires the sensitivity of ALMA. To date, only a handful of DSFGs have resolved ALMA imaging, but we can compare other tracers of the ISM until we have a larger ALMA sample. Rujopakarn et al. (2011) compiles from the literature ISM diameters for the GOALS sample measured from $Pani$, 8.4 GHz, and CO (3–2). The authors also compile CO (3–2) and 1.4 GHz sizes for galaxies in the GOODS-N field. The diversity of measurements underscores the need for a homogeneous ALMA comparison. The bottom panel of Figure 7 compares ISM diameter with $L_{\text{IR}}^{\text{SF}} / M_{\text{dust}}$. The GOALS DSFGs are all much smaller than the high-$z$ DSFGs. However, this does not translate to different $L_{\text{IR}}^{\text{SF}} / M_{\text{dust}}$ or $L_{160}^{\text{SF}} / L_{70}^{\text{SF}}$ ratios. This echoes the result in Lee et al. (2016), where the authors find that local dust-obscured galaxies, likely very compact, with $L_{\text{IR}} = 10^{11}$–$10^{12}$ have similar dust masses and temperatures as their less obscured, more extended counterparts. Similarly, using SEDs output from hydrodynamical simulations, Martínez-Galarza et al. (2016) recently found that mergers and compactness alone are not able to reproduce the SEDs of local LIRGs, but that increasing the gas fraction was required.

However, without a large sample of measurements of galaxy size in the dust continuum (i.e., with ALMA), it is very difficult to distinguish between size and $M_{\text{dust}}$ as the driver of the colder dust temperatures, since these effects are linked. Figure 7 clearly demonstrates that the high-$z$ galaxies are larger. If a galaxy can be represented as a central heating source surrounded by a disk of dust, then naturally a more extended disk will produce a lower $T_{\text{dust}}$, as the outskirts of the disk will see a diminished radiation field (e.g., Misselt et al. 2001). But, this is not a realistic description of most galaxies. Instead, to first order, both the SFR and dust densities are correlated with gas density, and so a mixed geometry of SFR regions within the ISM is more likely. In this geometry, the extent of the
system does not affect the global effective dust temperature (Misselt et al. 2001; Safarzadeh et al. 2016). How size and increased dust/gas mass are linked is also difficult to unravel. Locally, compaction can lead to a more efficient transformation of atomic gas into molecular gas (Larson et al. 2016), so a decrease in size could actually be the trigger of increased molecular gas masses in many of the GOALS galaxies (Díaz-Santos et al. 2010a, 2010b). Alternately, a smaller size translates to a higher SFR surface density, which would boost \( L_{\text{IR}}^{\text{SF}} \) without requiring a boost in \( M_{\text{gas}} \), leading to higher SFE at smaller size (Hayward et al. 2011, 2012). These effects are observed locally and in simulations, but our small sample of high-z galaxies do not appear to show any of the same trends between small size and higher temperatures or \( L_{\text{IR}}^{\text{SF}}/M_{\text{dust}} \). These galaxies also have optical radii measurements from the CANDELS collaboration, and we find no correlation between the optical radius measured in the observed frame \( H \)-band and \( L_{\text{IR}}^{\text{SF}}/M_{\text{dust}} \). On the other hand, Scoville et al. (2016) argue that high-z galaxies have more turbulent ISMs, leading to compression in the ISM and enhancing the SFE per unit mass. This efficient mode of star formation can occur throughout the galaxy, so no obvious correlation between galaxy size and dust temperature may be expected.

Local galaxies can be resolved, allowing their ISM geometry to be measured in more detail than high-redshift galaxies (e.g., Barcos-Muñoz et al. 2015). Given the quality and abundance of observations, it is more straightforward to link mergers with compact starbursts with dust heating in the GOALS samples (Díaz-Santos et al. 2010a). However, without resolved observations of the ISM in high-redshift galaxies, we see no obvious link between mergers, size, \( L_{\text{IR}}^{\text{SF}}/M_{\text{dust}} \), and \( f_{\text{dust}} \) in our sample. Therefore, we must conclude that a galaxy’s global far-IR/submillimeter emission, parameterized through \( L_{\text{IR}} \), \( f_{\text{dust}} \), \( M_{\text{dust}} \), or \( f_{\text{gas}} \) may not tell observers anything about the ISM geometry, extent, or merger stage of that galaxy.

6.3. The Effect of Increased Gas Fraction

There are two likely explanations for the observed increase in \( M_{\text{dust}} \) with redshift. The first is that DSFGs at \( z \sim 1–2 \) are simply more massive overall, that is, they have a higher stellar mass. \( M_{\ast} \) is expected to broadly scale with \( M_{\text{dust}} \), since a higher \( M_{\ast} \) in a DSFG implies a higher metallicity, supplying more metals to form dust in the ISM.

In Figure 8, we compare \( M_{\text{dust}} \) with \( M_{\ast} \). The three samples span the same range of \( \log M_{\ast} \sim 10–11.5 \ M_{\odot} \). However, the Supersample galaxies have roughly an order of magnitude higher dust masses. The solid, dotted, and dashed lines indicate how the relationship \( M_{\text{dust}} \) versus \( M_{\ast} \) is predicted to evolve with redshift using the semi-analytic models of Popping et al. (2016). We find an increase in \( M_{\text{dust}} \) with redshift larger than predicted by those models. The Supersample is offset from the GOALS galaxies by \( \sim 0.7 \) dex, which is the same amount of offset seen in the bottom panel of Figure 5. The Popping et al. (2016) models shown in our comparison are based on a semi-analytic model of galaxy formation in a cosmological context, which includes a standard suite of physical processes (gas accretion and cooling, star formation, stellar feedback, chemical enrichment, etc.). In addition, the Popping et al. (2016) model includes self-consistent tracking of the main processes thought to produce and destroy dust in galaxies, including dust condensation in stellar ejecta, dust growth through accretion in the ISM, dust destruction by supernovae, and ejection of dust by stellar-driven winds. The much milder evolution of \( M_{\text{dust}}/M_{\ast} \) with redshift predicted by these models relative to our findings is interesting, as it indicates that one or more of the model ingredients need to be revised.

The main sequence, which is the relationship between SFR and \( M_{\ast} \), evolves with redshift (e.g., Whitaker et al. 2012). That is, for a given \( M_{\ast} \), galaxies had a higher SFR at \( z \sim 1–2 \) than today. A higher SFR can be tied to an increase in dust mass indirectly, as the majority of grain growth is predicted to occur in the ISM, and a more gas-rich ISM will lead to higher dust masses and higher SFRs (e.g., Dwek 1998; Draine 2003; Santini et al. 2014; McKinnon et al. 2016a). The increased dust mass in the Supersample might then be a natural consequence of the increase in gas fractions with lookback time. As mentioned above, submillimeter data can also be converted to \( M_{\text{H}_{2}} \), and we use this parameterization to calculate gas fractions \( f_{\text{gas}} = M_{\text{H}_{2}}/M_{\ast} + M_{\text{H}_{2}} \). These gas fractions are consistent with what we derive using CO observations for several SMU5ES and Supersample galaxies (Yan et al. 2010; Kirkpatrick et al. 2014b).

We also calculate the distance of these galaxies from the main sequence. The main sequence evolves with redshift, and it flattens at higher \( M_{\ast} \). Therefore, we follow the method in Scoville et al. (2017) to calculate the main sequence. We use the relationship between \( M_{\ast} \) and SFR parameterized in Lee et al. (2015) at \( z = 1.2 \):

\[
\log \text{SFR}_{\text{MS}} = 1.72 - \log \left[ 1 + \left( \frac{M_{\ast}}{2 \times 10^{10} M_{\odot}} \right)^{-1.07} \right]. \tag{9}
\]
and then we renormalize depending on redshift (Speagle et al. 2014):

\[
\text{SFR}_{\text{MS}}(z) = \left( \frac{1 + z}{1 + 1.2} \right)^{1.2} \times \text{SFR}_{\text{MS}}(z = 1.2). \tag{10}
\]

Then, we calculate \(s\text{SFR} = \text{SFR}/M_\odot\) for every source and for the main sequence (MS) at each redshift.

We plot \(f_{\text{gas}}\) versus \(\Delta s\text{SFR} = s\text{SFR}/\text{SFR}_{\text{MS}}\) in the top panel of Figure 9. The Supersample is offset relative to the low-\(z\) samples, so that at a given \(\Delta s\text{SFR},\) the Supersample sources have higher gas fractions, consistent with previous results in the literature (Magdis et al. 2012; Genzel et al. 2015). This means that massive galaxies at \(z \sim 1.2\) have \(4-5\times\) higher gas fractions and hence gas masses, since the stellar masses are roughly consistent. Scoville et al. (2017) parameterize the evolution of the molecular gas mass as a function of redshift, \(M_{\text{HI}},\) and \(\Delta s\text{SFR.}\) In particular, the authors find that \(M_{\text{HI}}\) evolves as \((1 + z)^{3.84}\). For \(\log M_\odot = 10.7\ M_\odot\), and \(z = 0\) to \(z = 1.2\), we calculate the gas masses based on Equation (6) in Scoville et al. (2017) and overplot these predictions as the dashed and dotted-dashed lines. The predicted redshift evolution of \((1 + z)^{3.84}\) is consistent with our measurements, given the uncertainties in our stellar masses. This redshift evolution is best interpreted by also considering SFE, SFE \(\propto L_{\text{IR}}^{1/2}/M_{\text{dust}}^{1/2};\) massive dusty galaxies show little variation in metallicity, even at \(z \sim 1-2\), so a constant dust to gas ratio is a fair assumption (Magdis et al. 2012). We plot SFE versus \(\Delta s\text{SFR}\) in the bottom panel of Figure 9. The obvious correlation (Kendall’s \(\tau = 0.45\)) is similar to the well-established dependence of the gas depletion timescale \(t_{\text{dep}} = \text{SFE}^{-1}\) on \(s\text{SFR}\) (Saintonge et al. 2011; Magdis et al. 2012; Tacconi et al. 2013; Huang & Kauffmann 2014; Sargent et al. 2014). We overplot the relation derived in Genzel et al. (2015), where the authors use CO observations to calculate molecular gas mass for 500 SFGs from \(z = 0-3\). There is no offset in any of our samples, consistent with the very mild redshift evolution between \(t_{\text{dep}}\) and \(\Delta s\text{SFR}\) found by Genzel et al. (2015). However, this is in contrast to Scoville et al. (2017), who measure an increase in SFE \(\propto (1 + z)^{0.05}\) for a given stellar mass. We plot what this evolution looks like using the arrow in the lower right corner for \(z = 0\) to \(z = 1.2,\) and \(\log M_\odot = 10.7\ M_\odot.\)

The clear increase in gas fractions with redshift, without corresponding increases in SFE, suggests that the higher SFRs (corresponding to higher \(L_{\text{IR}}\)) and higher \(M_{\text{dust}}\) of the Supersample at \(z \sim 1-2\) are driven by an increase in the gas supply rather than an increase in SFR or \(M_\odot,\) or a changing mode of star formation with cosmic time (Bouché et al. 2010; Davé et al. 2012; Tacconi et al. 2013; Genzel et al. 2015; Schinnerer et al. 2016). In fact, the bottom panel of Figure 5 demonstrates that at a given \(L_{\text{IR}}^{1/2}\) (SFR), SFEs are lower at \(z \sim 1-2,\) this increase in gas supply is also predicted by the underlying cause of the main-sequence evolution, SFR/\(M_\odot,\) with redshift (Bouché et al. 2010; Davé et al. 2012; Tacconi et al. 2013; Genzel et al. 2015). We can directly test whether an increase in \(f_{\text{gas}}\) fully explains the increase in \(M_{\text{dust}}\) using the relationship between \(f_{\text{gas}}\) and \(z,\) parameterized as \(f_{\text{gas}} = 0.1(1 + z)^2\) (Geach et al. 2011). If we assume a dust-to-gas ratio of 100 and \(\log M_\odot = 10.7\ M_\odot,\) then at \(z = 0,\) \(\log M_{\text{dust}} = 7.75\ M_\odot,\) and at \(z = 1.2,\) \(\log M_{\text{dust}} = 8.67\ M_\odot.\) These predictions are plotted as the dark filled symbols in Figure 8, and they agree remarkably well with GOALS and the Supersample.

7. Conclusions

We have analyzed the far-IR/submillimeter properties of three samples of IR luminous galaxies. We combine GOALS and SMUSES galaxies to form a low-\(z\) sample (\(z < 0.3\), and the Supersample comprises our high-\(z\) sample (\(z \sim 0.5-2\)). Mid-IR spectra are available for every source, and we utilize these spectra to identify sources with a hot dust continuum, likely due to an AGN, and remove them from the sample. We measure \(L_{250}/L_{70},\ L_{160}/L_{70},\ L_{dust},\) and \(f_{\text{gas}}\) self-consistently for all galaxies. We find:

1. \(L_{250}/L_{70}^{SF}\) is tightly correlated with \(L_{160}/L_{70}^{SF}\) for all galaxies and both ratios are sensitive to the strength of the ISRF, as parameterized by SED models. The low-\(z\) and high-\(z\) samples span the same range of colors, although...
for a given \( \frac{L_{160}^{\text{SF}}}{L_{70}^{\text{SF}}} \), the high-z galaxies have a higher \( \frac{L_{250}^{\text{SF}}}{L_{70}^{\text{SF}}} \), indicating that they have proportionally more cold dust.

2. \( \frac{L_{160}^{\text{SF}}}{L_{70}^{\text{SF}}} \) is correlated with \( L_{\text{IR}}^{\text{SF}} \), but this relationship evolves with redshift so that at \( z \sim 1-2 \), DSFGs are \( \sim 5 \) K colder.

3. There is a strong relationship between \( L_{\text{IR}}^{\text{SF}} / M_{\text{dust}} \) and \( L_{\text{IR}}^{\text{SF}} \), and this relationship evolves with redshift. DSFGs at \( z \sim 1-2 \) have \( L_{\text{IR}}^{\text{SF}} / M_{\text{dust}} \) ratios similar to low-z galaxies a factor of \( 5 \) less luminous. DSFGs also have higher dust masses than their local counterparts at the same luminosity.
4. The relationship between $M_{\text{dust}}$ and $M_*$ also evolves strongly with redshift, so that DSFGs at $z \sim 1$--2 have a greater than factor of 5 higher $M_{\text{dust}}$ than local DSFGs in the same $M_*$ range. This mirrors the measured increase in gas fraction with redshift from other studies.

5. We observe a redshift-independent correlation between distance from the main sequence ($\Delta sSFR$) and SFE. The higher star formation rates (corresponding to higher $L_{\text{IR}}$) in our $z \sim 1$--2 sample are then fueled by an increase in their gas content, rather than an increase in SFE.
6. We see a tight redshift-independent correlation between $L_{\text{IR}}^{\text{SF}}$ and $L_{160}^{\text{SF}}$, which is a proxy for $T_{\text{dust}}$. We see no correlation between merger classification and either $L_{\text{IR}}^{\text{SF}}$ or $L_{160}^{\text{SF}}$. This is also true of galaxy size. Then, the change to colder $T_{\text{dust}}$ in high-$z$ DSFGs can be explained simply by an increase in dust mass at fixed $L_{\text{IR}}^{\text{SF}}$, without requiring any change in the merger fraction or extent of the ISM, although this may be a related effect.

7. In the subsample of galaxies for which we have size measurements, the large galaxy sizes at high $z$ and lack of a correlation between size and $L_{160}/L_{70}$ favor an ISM
geometry in which the stars and dust are well mixed, so the expectation based on a central source surrounded by dust (that $T_{\text{dust}}$ is inversely proportional to size) does not hold.

8. The far-IR/submillimeter SED can be fully parameterized in terms of the observables $L_{\text{IR}}$, $L_{\text{SF}}^{160}$, $L_{\text{SF}}^{70}$ or, alternatively, the dust mass and the luminosity absorbed by dust (which is equal to $L_{\text{IR}}$ unless dust self-absorption is non-negligible). As such, a galaxy’s global far-IR/submillimeter emission alone cannot be used to distinguish between ISM geometries.

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Appendix A
Rest-frame Photometry

In Figure 10 we plot the IR/submillimeter SEDs of the Supersample galaxies listed in Table 1. We also plot the estimated rest-frame 70, 160, 250 μm photometry. For two galaxies, GN_IRS49 and MIPS8543, we do not have enough coverage at $\lambda > 200 \mu m$ to reliably estimate a rest-frame $L_{250}$. The errors on the estimated rest-frame photometry are largely attributable to the uncertainties on the templates (Kirkpatrick et al. 2013b) used to derive the photometry.

Appendix B
Dust Mass Calculations

We explore how trends between $L_{\text{IR}}^{\text{SF}}$ and $M_{\text{dust}}$ will change if we use different $T_{\text{dust}}$ to calculate $M_{\text{dust}}$.

Determining a dust temperature from the SED involves fitting a modified blackbody to the far-IR data. This temperature is then a luminosity-weighted temperature that may not represent the true temperature of the bulk of the dust mass. Instead, the effective dust temperature probes the mean ionization parameter $U$ “seen” by the dust (Draine & Li 2007). If a single modified blackbody is used, $T_{\text{dust}}$ is measured using all far-IR photometry, but below $\lambda < 100 \mu m$, dust is being heated primarily in star-forming regions, as opposed to the diffuse dust in the ISM heated by the interstellar radiation field (Lonsdale Persson & Helou 1987; Dunne & Eales 2001). Dust masses calculated from a one-temperature modified blackbody can underestimate the true dust mass by at least a factor of 2 (Magdis et al. 2012). The cold diffuse component is what makes up the bulk of the dust mass. $T_{\text{cold}}$ is often measured by
fitting a two-temperature modified blackbody (e.g., Dunne & Eales 2001; Kirkpatrick et al. 2012; Lee et al. 2016), but this method requires full sampling of the far-IR SED or assumptions about \( \beta \) and the warm dust component, not to mention that the model is unphysical.

We now explore trends in dust mass when the dust temperature of the diffuse ISM is assumed to scale with increasing \( L_{\text{IR}}^{\text{SF}} \), as this is consistent with what would be measured by fitting a one-temperature modified blackbody to the SED (e.g., Blain et al. 2003; Chapman et al. 2003; Chapin et al. 2009; Casey et al. 2012; Lee et al. 2016). We calculate \( T_{\text{dust}} \) according to

\[
T_{\text{dust}} = 0.47 \times (L_{\text{IR}}^{\text{SF}})^{0.144},
\]

determined from 767 SPIRE 250 \( \mu \)m selected sources spanning \( z = 0-5 \), where \( T_{\text{dust}} \) was calculated from the peak wavelength of the SED (Casey et al. 2012); we ignore the redshift evolution of the normalization for the time being. The left panel of Figure 11 shows \( M_{\text{dust}} \) as a function of \( L_{\text{IR}}^{\text{SF}} \). There is an overall trend toward increasing \( M_{\text{dust}} \) with increasing \( L_{\text{IR}}^{\text{SF}} \), although for the the Supersample, \( M_{\text{dust}} \) is nearly constant over two orders of magnitude in \( L_{\text{IR}}^{\text{SF}} \). The Supersample is offset from the GOALS and 5MUSES sample, with higher \( M_{\text{dust}} \) at similar \( L_{\text{IR}}^{\text{SF}} \), confirming the trend in Figure 5.

The GOALS and 5MUSES galaxies lie decidedly below the Supersample galaxies, and this is not explained by the evolution in the \( L_{\text{IR}}-T_{\text{dust}} \) relation with redshift. We can test for the effect of redshift by instead using the \( L_{\text{IR}}-T_{\text{dust}} \) relation derived from local IRAS BGS sources, which we approximate as \( T_{\text{dust}} \propto (L_{\text{IR}}^{\text{SF}})^{0.137} \) (Chapman et al. 2003; Casey et al. 2012). When we apply the IRAS BGS relation to the 5MUSES and GOALS galaxies, they lie around the dotted line in Figure 11. Rather than bringing the low-\( z \) and high-\( z \) samples into better agreement, using two \( L-T \) relations will make the dust masses more discrepant.

Alternately, we can calculate \( T_{\text{dust}} \) and \( \beta \) through template fitting. The Dale et al. (2014) library, which we use to approximate the far-IR colors of our galaxies in Figure 3, has an effective \( T_{\text{dust}} \) and \( \beta \) associated with each template. We fit the Dale et al. (2014) library to all sources using a \( \chi^2 \)-minimization technique. We then use the best-fit template \( \beta \) to scale \( \kappa \) as

\[
\kappa_{\lambda} = \kappa_{850} \times \left( \frac{850}{\lambda} \right)^{\beta},
\]

where \( \kappa_{850} = 0.15 \text{ m}^2 \text{ kg}^{-1} \) (Weingartner & Draine 2001) and \( \lambda \) is the submillimeter wavelength we calculate dust mass at for each galaxy. We use the \( \kappa_{\lambda} \) and \( T_{\text{dust}} \) associated with the best-fit template to calculate \( M_{\text{dust}} \). The results are shown in the right panel of Figure 11. Again, the same increase in \( M_{\text{dust}} \) with redshift for a given \( L_{\text{IR}}^{\text{SF}} \) is seen. The only difference is that now, at a given \( L_{\text{IR}}^{\text{SF}} \), the low-\( z \) galaxies have \( \log L_{\text{IR}}^{\text{SF}}/M_{\text{dust}} \) that is 0.8 dex below the high-\( z \) galaxies, slightly larger than the 0.7 dex offset in Figure 5. We conclude that the observed evolution of \( L_{\text{IR}}^{\text{SF}}/M_{\text{dust}} \) with redshift is real and not a product of how we are deriving dust masses.

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