Coarse-Grained Simulation of the Adsorption of Water on Au(111) Surfaces Using a Modified Stillinger–Weber Potential

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ABSTRACT: For reproducing the behavior of water molecules adsorbed on gold surfaces in terms of density of both bulk and interfacial water and in terms of structuring of water on top of gold atoms, the implementation of a multibody potential is necessary, thus the Stillinger–Weber potential was tested. The goal is using a single nonbonded potential for coarse-grained models, without the usage of explicit charges. In order to modify the angular part of the Stillinger–Weber potential from a single cosine to a piecewise function accounting for multiple equilibrium angles, employed for Au–Au–Au and Au–Au–water triplets, it is necessary to create a version of the simulation package LAMMPS that supports the assignment of multiple favored angles. This novel approach is able to reproduce the data obtained using quantum mechanical calculations and density profiles of both bulk and adsorbed water molecules obtained using classical polarizable force fields.

1. INTRODUCTION

In the last few years, in nanoscience, the use of functionalized nanoparticles with biomolecules has gained a lot of interest, with applications in drug delivery,1 theranostics,2 heterogeneous catalysis,3 and clinical4 and environmental5 analyses. Functionalization is possible by using covalently bonded molecules on Au surfaces by means of thiol groups. Noncovalent passivation is also used in water media to functionalize Au surfaces.6 With the aim of studying these systems with classical molecular dynamics simulations, traditional force fields using exclusively two-body potentials for the nonbonded interactions are no longer effective. An important example is the simple adsorption of water on the Au(111) surface. Density functional theory (DFT) calculations state that a single water molecule has to be on top, forming an angle of 90° with two Au surface atoms and that hydrogen atoms do not have to point directly to the Au surface.7 These results cannot be reproduced by using only two body terms, even if we are talking about water models at full atomistic resolution (including electrostatics). In fact, calculations performed using a nonbonded attractive-repulsive two-body term for the interaction of a single water molecule with a face centered cubic (FCC) Au(111) surface will give rise to a large free-energy minimum on the “hollow” site (because of the contribution from interactions with three surface atoms).

To overcome this problem, a multibody potential becomes necessary and the three-body Stillinger–Weber Potential (SWP) can be successfully used. SWP parameters for water molecules in bulk,8 polyethylene,9 and organic solutes10 in water are already present in the literature. In the latter case, the authors were able to reproduce the potential of mean force (PMF) of a methane dimer in water, establishing a basis for a CG force-field for aqueous soft matter systems based only on nonbonded interaction without electrostatic contributions. Other examples of efficient usage of the SWP are the original works on silicon,11 gallium,12 tetrahedral carbon,13 and other elements in a cubic lattice.14 Furthermore, other CG applications with SWP exist for calcite/water nucleation-growth mechanisms.15 An implementation of three-body interactions, coupled with a polarizability term in the two-body function, has been successfully used in classical molecular dynamics simulations, in full atomistic representation, for the adsorption of water on Au surfaces.16

Full atomistic models using electrostatic interactions alongside a fully parametrized three body term for the physisorption or chemisorption of water on noble metal 111 surfaces are reported by Steinmann et al.17 and Clabaut et al.18

As far as we know, a simulation model for the adsorption of water on an Au surface using a CG approach and without any explicit polarizability and/or electrostatic term does not exist so far.
In this article, we searched for an accurate description of the interaction between water molecules represented by the Molinero water (mW) model and an FCC Au(111) surface, parameterizing Au and water two- and three-body interactions in a modified version of the SWP for CG molecular dynamics simulations.

The SWP functional form (eq 1) is explicitly separable in two parts: an attractive-repulsive term for the two-body interaction (eq 2) and a purely repulsive three-body angular dependence (eq 3)

\[ V_{SW}(r) = \sum_i \sum_{j>i} \varphi_2(r_{ij}) + \sum_i \sum_{j>i} \sum_{k>j} \varphi_3(r_{ijk}, r_k, \cos \theta_{ijk}) \]  

\[ \varphi_2(r_{ij}) = \begin{cases} A_{ij} \left( B_{ij} \left( \frac{\sigma_{ij}}{r_{ij}} \right)^4 - 1 \right) \exp \left( \frac{1}{\sigma_{ij} - a_{ij}} \right), & r_{ij} < a_{ij} \\ 0, & r_{ij} \geq a_{ij} \end{cases} \]  

\[ \varphi_3(r_{ij}, r_k, \cos \theta_{ijk}) = \begin{cases} \lambda_{ijk} \varepsilon_{ijk} (\cos \theta_{ijk} - \cos \theta_{ij})^2 & \frac{r_{ij}}{\sigma_{ij}} < a_{ij} \\ \exp \left( \frac{\gamma_{ij}}{\sigma_{ij} - a_{ij}} + \frac{\gamma_{jk}}{\sigma_{jk} - a_{jk}} \right) & \frac{r_{ij}}{\sigma_{ij}} \geq a_{ij} \end{cases} \]  

Here, \( A_{ij} \) and \( \lambda_{ijk} \) are the strengths of the two-body and three-body interactions and alongside \( B_{ij}, \sigma_{ij}, a_{ij} \) represent the full set of parameters to completely describe the SWP. \( \varepsilon_{ijk} = \varepsilon_{ij} = \varepsilon_{ji} \) according to the LAMMPS definition.

In particular, for the two-body function (\( \varphi_2 \)), it is possible to optimize the parameters in order to reproduce the force constant, energy minimum, and equilibrium distance, matching the zeroth, first, and second derivatives of the potential (eq 4), calculated at the equilibrium value (\( r = r_e \)).

\[ \left( \frac{\partial \varphi_2}{\partial \sigma} \right)_{r_e} = 0 \rightarrow B \left( \frac{r_e}{\sigma}, a \right) = \frac{\left( \frac{\varepsilon}{\sigma} \right)^4}{4 \left( \frac{\varepsilon}{\sigma} - a \right)^2} + 1 \]  

\[ \varphi_2(r_e) = -\epsilon \rightarrow A \left( \frac{r_e}{\sigma}, a \right) = \frac{\exp \left( \frac{1}{a - \sigma} \right)}{1 - \left( \frac{\varepsilon}{\sigma} \right)^2 B \left( \frac{\varepsilon}{\sigma}, a \right) \left( \frac{\varepsilon}{\sigma} - a \right)^2} \]  

\[ \left( \frac{\partial^2 \varphi_2}{\partial \sigma^2} \right)_{r_e} = k \left( \frac{r_e}{\sigma}, a \right) \]  

With this approach, the large number of parameters in the SWP can be reduced to only two quantities, namely \( r_e/\sigma \) and \( a \).

2. METHODS
All the simulations have been performed using the simulation package LAMMPS with a 5 fs time step in the isothermal–isobaric (NPT) ensemble with a semi-isotropic pressure coupling. Temperature and pressure were controlled using a Nose–Hoover thermostat and a barostat using 100 fs, and 1 ps damping constants, for temperature and pressure, respectively. The equilibrium external pressures were 0, 0, and 1 atm for \( X, Y, \) and \( Z \), respectively, where \( Z \) is the axis normal to the Au surface. The simulations were performed by using a box (\( 5 \times 5 \times 9 \) nm\(^2\)) containing a slab of 2880 Au atoms (FCC) and 5785 water molecules and applying the periodic boundary conditions.

A piecewise function for the angular dependence of the SWP has been implemented in C++ as a new pair style (link for LAMMPS downloadable input files and for the modified code: https://github.com/gripani/LAMMPSinput_file and https://github.com/gripani/LAMMPSBuild_SWmod). Analysis of the simulations has been performed by means of homemade programs.

3. RESULTS AND DISCUSSION
The parameters for the water-Au pair have been refined to reproduce the a posteriori feature (mass density) of the GollP-CHARMM polarizable force field.

The parameters for the Au bulk concerning the two-body part only have been obtained starting from the cohesive energy (\( E_C = \epsilon \)), lattice parameter (\( a_{BB} = r_e \sqrt{2} \)), and bulk modulus (\( B = \frac{2}{3} k_e \)) already existing in the literature. According to Molinero, the tetrahedrality of bulk water is \( \gamma = 1.2 \) for all the possible triplets in the system. According to Molinero, the tetrahedrality of bulk water is provided by \( \cos \theta_B = -1/3 \) and \( \lambda = 23.15 \). Concerning the Au FCC lattice in the bulk phase, it is not possible to reproduce the three-body energy using a single value of the equilibrium angle. The same issue, with more critical aspects, appears in the case of the mW–Au–Au triplet as well.

Indeed, one adsorbed water and its nearest neighbor Au atom, for the FCC lattice, form an angle of 90° with an Au atom of the first layer and an angle of 144.7° with a nearest neighbor Au of the second layer (Figure 1).

Figure 1. Schematic representation of the two different angles formed by the normal to the Au surface and two adjacent Au atoms, connected by red lines (corresponding to the Au–Au equilibrium distance). The 90° angle is shown in light green and the 144.7° angle is shown in violet.
The functional form of the piecewise function (eq 5) concerning N different equilibrium angles is given as follows ($x_n^{\text{min}}$ and $x_n^{\text{max}}$ are the limiting values of the n-th piece interval)

$$g(\cos \theta) = \left( g_0^0 + (-1)^{n+1} (\cos \theta - \cos \theta_0^0)^2 \right); x_n^{\text{min}} \leq \cos \theta < x_n^{\text{max}}$$

In Table 2, the parameters of the piecewise function for an FCC lattice are reported. The same g function with modified parameters (reported in Table 3) can also be used to describe the behavior of water molecules interacting with the Au atoms, assuring the preferential top site geometry.

In order to implement the modified angular dependence for the multilayer approach, we defined a new style in the LAMMPS source code (SWPmod).

Specifically, the pairwise function $g(\cos \theta)$ (eq 5) goes in place of $(\cos \theta_{\text{ij}} - \cos \theta_0^0)^2$ in the three-body function (eq 3).

Because of technical reasons, we have introduced in our code a switch parameter, with the role of choosing which piecewise function is necessary for which triplet (alongside the full set of parameters $n, x_n^{\text{min}}, x_n^{\text{max}}, \cos \theta_0^0$ and $g_0^0$). In this way, the approach can be easily extended to other molecular systems. In particular, if switch = 0, no piecewise function will be used (single-angle harmonic cosine function); if switch = 1, the two angle piecewise function will be used for the mW, Au, Au triplet, as reported in Table 2; if switch = 2 the four angle piecewise function will be used (for bulk Au as reported in Table 1).

It is noteworthy that it is possible to realize a fine tuning of the correct top site configuration by changing the strength of the repulsive three-body term ($\lambda$) for the mW−Au−Au triplet. Figure 2 (top) shows the average orientation of water molecules with respect to the Au surface sites. The figure nicely illustrates how it is possible to shift the equilibrium configuration of the adsorbed water molecules from the hollow to the top sites, performing NPT simulations with different $\lambda$ values (Table 4).

From the water density in the $z$-direction (i.e., normal to the surface), the PMF of the adsorption of the water molecules on the Au surface can be obtained (eq 6).

The two minima correspond to the first and second layers of the adsorbed molecules, from which it is possible to estimate both equilibrium (eq 7) and kinetic (eq 8) constants of the exchange process between the two layers (corresponding to the first and second minima of Figure 3 in the case $\lambda = 50$).
\[ \beta W(Z) = -\log \left( \frac{\rho(Z)}{\rho(\infty)} \right) \]  
(6)

\[ K_{eq} = \exp(-\beta \Delta W^0) = 1.82 \]  
(7)

\[ k = (\beta \hbar)^{-1} \exp(-\beta \Delta W^0) = 1.14 \text{ ps}^{-1} \]  
(8)

\[ \Delta W^0 \] is the difference between the values of the PMF of the first and the second minimum and \( \Delta W^0 \) is the difference between the value of the PMF calculated at the first maximum and the value of the PMF calculated at the first minimum. In the Eyring equation (eq 8), the transmission coefficient is set equal to 1, as it is usually assumed for transport processes.

4. CONCLUSIONS

In conclusion, with the support of a multibody potential, we were able to reproduce the correct configuration of the adsorbed water molecules on the Au(111) surface and the water density profile as obtained using the GolP-CHARMM force field. The model is also able to describe the first and second layers of the adsorbed water molecules. The advantages of this approach are the absence of explicit partial charges so that it does not need any electrostatic contribution on the energy and the reduced number of simulated particles with the CG approach. In contrast, the GolP-CHARMM force field makes use of explicit dummy charges bound to Au atoms and is fully atomistic. Finally, the versatility and general form of the three-body part of the Stillinger–Weber potential allows a possible extension of the proposed approach to other molecular systems.

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REFERENCES

(1) Ferris, D. P.; Lu, J.; Gothard, C.; Yanes, R.; Thomas, C. R.; Olsen, J.-C.; Stoddart, J. F.; Tamanoi, F.; Zink, J. I. Synthesis of biomolecule-modified mesoporous silica nanoparticles for targeted hydrophobic drug delivery to cancer cells. Small 2011, 7, 1816−1826.
(2) Biscaglia, F.; Ripani, G.; Rajendran, S.; Benna, C.; Mocellin, S.; Bocchinfuso, G.; Meneghetti, M.; Palleschi, A.; Gobbo, M. Gold Nanoparticle Aggregates functionalized with cyclic RGD peptides for targeting and imaging of colorectal cancer cells. ACS Appl. Nano Mater. 2019, 2, 6436−6444.
(3) Roy, S.; Pericás, M. A. Functionalized nanoparticles as catalysts for enantioselective processes. Org. Biomol. Chem. 2009, 7, 2669−2677.
(4) Anselmo, A. C.; Mitragotri, S. Nanoparticles in the clinic. Bioeng. Transl. Med. 2016, 1, 1−29.
(5) Kolataj, K.; Krajcewska, J.; Kudelski, A. Plasmonic nanoparticles for environmental analysis. Environ. Chem. Lett. 2020, 18, 529−542.
(6) Hughes, Z. E.; Walch, T. R. Non-covalent adsorption of amino acid analogues on noble-metal nanoparticles: influence of edges and vertices. Phys. Chem. Chem. Phys. 2016, 18, 17525.
(7) Berg, A.; Peter, C.; Johnston, K. Evaluation and Optimization of Interface Force Fields for Water on Gold Surfaces. J. Chem. Theory Comput. 2017, 13, 5610−5623.
(8) Molinero, V.; Moore, E. B. Water modeled as an intermediate element between carbon and silicon. J. Phys. Chem. B 2009, 113, 4008−4016.
(9) Raubenhoit, B.; Gyalwali, G.; Tang, W.; Wong, K. S.; Rick, S. W. Coarse-Grained Simulations of Aqueous Thermoresponsive Poly-ethers. Polymers 2018, 10, 475.
(10) Molinero, V.; Song, B. Thermodynamic and structural signatures of water-driven methane-methane attraction in coarse-grained mW water. J. Chem. Phys. 2013, 139, 054511.
(11) Stillinger, F. H.; Weber, T. A. Computer simulation of local order in condensed phases of silicon. Phys. Rev. B: Condens. Matter Mater. Phys. 1985, 31, 5262.
(12) Béré, A.; Serra, A. On the atomic structures, mobility and interactions of extended defects in GaN: dislocations, tilt and twin boundaries. Philos. Mag. A 2006, 86, 2159−2192.
(13) Barnard, A. S.; Russo, S. P. Development of an improved Stillinger-Weber potential for tetrahedral carbon using ab initio (Hartree-Fock and MP2) methods. Mol. Phys. 2002, 100, 1517−1525.
(14) Zhou, X. W.; Wedley, H. N. G. A potential for simulating the atomic assembly of cubic elements. Comput. Mater. Sci. 2007, 39, 340−348.
(15) King, M.; Pasler, S.; Peter, C. Coarse-Grained Simulation of CaCO3Aggregation and Crystallization Made Possible by Non-bonded Three-BodyInteractions. J. Phys. Chem. C 2019, 123, 3152−3160.
(16) Siepmann, J. I.; Sprik, M. Influence of surface topology and electrostatic potential on water/electrodesystems. J. Chem. Phys. 1995, 102, 511.
(17) Steinmann, S. N.; Ferreira De Morais, R.; Götz, A. W.; Fleurat-Lessard, P.; Iannuzzi, M.; Sautet, P.; Michel, C. Force Field for Water
over Pt(111): Development, Assessment, and Comparison. *J. Chem. Theory Comput.* 2018, 14, 3238–3251.

(18) Clabaut, P.; Fleurat-Lessard, P.; Michel, C.; Steinmann, S. N. Ten Facets, One Force Field: The GAL19 Force Field for Water−Noble Metal Interfaces. *J. Chem. Theory Comput.* 2020, 16, 4565–4578.

(19) Plimpton, S. Fast Parallel Algorithms for Short-Range Molecular Dynamics. *J. Comp. Physiol.* 1995, 117, 1–19.

(20) Evans, D. J.; Holian, B. L. The Nose-Hoover thermostat. *J. Chem. Phys.* 1985, 83, 4069.

(21) Wright, L. B.; Rodger, P. M.; Corni, S.; Walsh, T. R. GolP-CHARMM: First-Principles Based Force Fields for the Interaction of Proteins with Au(111) and Au(100). *J. Chem. Theory Comput.* 2013, 9, 1616–1630.

(22) Ambrosetti, A.; Silvestrelli, P. L. Cohesive properties of noble metals by van der Waals-corrected Density Functional Theory. *Phys. Rev. B* 2016, 94, 045124.