Abstract

We present a new direction for increasing the interpretability of deep neural networks (DNNs) by promoting weight-input alignment during training. For this, we propose to replace the linear transforms in DNNs by our B-cos transform. As we show, a sequence (network) of such transforms induces a single linear transform that faithfully summarises the full model computations. Moreover, the B-cos transform introduces alignment pressure on the weights during optimisation. As a result, those induced linear transforms become highly interpretable and align with task-relevant features. Importantly, the B-cos transform is designed to be compatible with existing architectures and we show that it can easily be integrated into common models such as VGGs, ResNets, InceptionNets, and DenseNets, whilst maintaining similar performance on ImageNet. The resulting explanations are of high visual quality and perform well under quantitative metrics for interpretability. Code available at github.com/moboehle/B-cos.

1. Introduction

While deep neural networks (DNNs) are highly successful in a wide range of tasks, explaining their decisions remains an open research problem [29]. The difficulty here lies in the fact that such explanations need to faithfully summarise the internal model computations and present them in a human-interpretable manner. E.g., it is well known that piece-wise linear models (e.g., ReLU-based [24]) are accurately summarised by a linear transform for every input [23]. However, despite providing an accurate summary, these piece-wise linear transforms are generally not intuitively interpretable for humans and typically perform poorly under quantitative interpretability metrics, cf. [32, 43]. Recent work thus aimed to improve the explanations’ interpretability, often focusing on their visual quality [2]. However, gains in the visual quality of the explanations often came at the cost of their model-faithfulness [2].

Instead of optimising the explanation method, in this work we aim to optimise the DNNs to inherently provide an explanation that fulfills the aforementioned requirements—the resulting explanations constitute both a faithful summary and have a clear interpretation for humans. For this, we propose the B-cos transform as a drop-in replacement for linear transforms. As such, the B-cos transform can easily be integrated into a wide range of existing DNN architectures and we show that the resulting B-cos DNNs provide high-quality explanations for their decisions, see Fig. 1.

To ensure that these explanations constitute a faithful summary of the models, we design the B-cos transform as an input-dependent linear transform. Importantly, any sequence of such transforms therefore induces a single linear transform that faithfully summarises the entire sequence. In order to make the induced linear transforms interpretable, the B-cos transform is designed to induce alignment pressure on the weights during optimisation, which optimises the model weights to align with task-relevant input patterns. The linear transform induced by the model thus has a clear interpretation: it is a direct reflection of the weights the model has learnt during training and specifically reflects those weights that best align with a given input.

In summary, we make the following contributions:

1. We introduce the B-cos transform to improve neural network interpretability. By promoting weight-input align-
ment, these transforms are explicitly designed to yield explanations that highlight task-relevant patterns in the input. (2) Specifically, the B-cos transform is designed such that any sequence of B-cos transforms can be faithfully summarised by a single linear transform. We show that this allows to explain not only the models’ output neurons, but also neurons from arbitrary intermediate network layers.

(3) We demonstrate that a plain B-cos convolutional neural network without any additional non-linearities, batch-norm layers [15], or regularisation schemes can achieve competitive performance on CIFAR10 [18]. In an ablation study we also show that the parameter B allows for fine-grained control over the increase in weight alignment and thus the interpretability of the B-cos networks.

(4) To highlight the generality of our approach, we show that the B-cos transform can easily be integrated into various commonly used DNNs such as InceptionNet [39], ResNet [13], VGG [34], and DenseNet [14] models, whilst maintaining similar performance. More importantly, the resulting architectures are highly interpretable under the B-cos explanations and outperform other explanation methods across all tested architectures, both under quantitative metrics as well as under qualitative inspection.

2. Related work

Approaches for understanding DNNs typically focus on explaining individual model decisions post-hoc, i.e., they are designed to work on any pre-trained DNN. Examples of this include perturbation-based, [21, 26, 28], activation-based, [8, 17], or backpropagation-based explanations, [3, 30, 32, 33, 35, 36, 38, 44]. In order to obtain explanations for the B-cos networks, we also rely on a backpropagation-based approach. In contrast to post-hoc explanation methods, however, we optimise the B-cos networks to be explainable under this particular form of backpropagation and the resulting explanations are thus model-inherent.

The design of such inherently interpretable models has gained increased attention recently. Examples include prototype-based networks [7], BagNets [5], and CoDA Nets [6]. Similar to the BagNets and the CoDA Nets, our B-cos networks can be faithfully summarised by a single linear transform. Moreover, similar to [6], we rely on a structurally induced alignment pressure to make those transforms interpretable. In contrast to those works, however, our method is specifically designed to be compatible with existing neural network architectures, which allows us to improve the interpretability of a wide range of DNNs.

Weight-input alignment in DNNs has recently received increased attention. E.g., it has been observed that adversarial training promotes alignment [40] and recent studies suggest that this could increase interpretability via gradient-based explanations [16, 31]. Further, [37] introduce a loss to increase alignment. Instead of relying on loss-based model regularisation, the increase in alignment in B-cos networks is based on architectural constraints that require weight-input alignment for solving the optimisation task.

Non-linear transforms. While the linear transform is the default operation for most neural network architectures, many non-linear transforms have been investigated, [11, 19, 20, 22, 42, 45]. Most similar to our work are [19, 20, 22], which assess transforms that emphasise the cosine similarity (i.e., ‘alignment’) between weights and inputs to improve model performance. In fact, we found that amongst other transforms, [19] evaluates a non-linear transform that is equivalent to our B-cos operator with B=2. In contrast to [19], we explicitly introduce this non-linear transform to increase interpretability and show that such models can be scaled to large-scale classification problems.

3. B-cos neural networks

In this section, we introduce the B-cos transform as a replacement for the linear units in DNNs, which are (almost) “at the heart of every deep network” [27], and discuss how this can increase the interpretability of DNNs.

For this, we first introduce the B-cos transform as a variation of the linear transform in Sec. 3.1 and highlight its most important properties. In Sec. 3.2, we show how to construct B-cos networks and how to faithfully summarise the network computations to obtain explanations for their outputs (3.2.1). Then, we discuss how the B-cos transform—combined with the binary cross entropy (BCE) loss—affects the parameter optima of the models (3.2.2). Specifically, by inducing alignment pressure, the B-cos transform aligns the model weights with task-relevant patterns in the input. Finally, in Sec. 3.3 we integrate the B-cos transform into conventional DNNs by using it as a drop-in replacement for the ubiquitously used linear units.

3.1. The B-cos transform

Typically, the individual ‘neurons’ in a DNN compute the dot product between their weights $w$ and an input $x$: $f(x; w) = w^T x = ||w|| ||x|| c(x, w)$, (1)

with $c(x, w) = \cos(\angle(x, w))$. (2)

Here, $\angle(x, w)$ returns the angle between the vectors $x$ and $w$. In this work, we seek to improve the interpretability of DNNs by promoting weight-input alignment during optimisation. To achieve this, we propose the B-cos transform:

$$
\text{B-cos}(x; w) = \left\{ \begin{array}{ll} ||\hat{w}|| ||x|| c(x, \hat{w})^B \times \text{sgn}(c(x, \hat{w})) & \text{if } B \neq 2 \\
|c(x, w)| & \text{if } B = 2 
\end{array} \right. .
$$

(3)

Here, B is a hyperparameter, the hat-operator scales $\hat{w}$ to unit norm, and sgn denotes the sign function. Note that this only introduces minor changes (highlighted in blue) with
respect to Eq. (1); e.g., note that for $B = 1$, the B-cos transform is equivalent to a linear transform with $\tilde{w}$. However, albeit small, these changes are important for three reasons. 

**First**, they bound the output of B-cos neurons, i.e.,

$$
\|\tilde{w}\| = 1 \Rightarrow \text{B-cos}(x; w) \leq \|x\|. \tag{4}
$$

As becomes clear from Eq. (3), equality in Eq. (4) is only achieved if $x$ and $w$ are collinear, i.e., aligned. 

**Secondly**, by increasing the exponent $B$, the output for badly aligned weights can be further suppressed,

$$
B \gg 1 \land |c(x, \tilde{w})| < 1 \Rightarrow \text{B-cos}(x; w) \ll \|x\|, \tag{5}
$$

and the respective B-cos unit can only produce outputs close to its maximum (i.e., $\|x\|$) for a small range of angular deviations from $x$. In combination, these two properties can significantly alter the optimality of the weight vectors $w$. To illustrate this, we show in Fig. 2 how increasing $B$ affects a simple linear classification problem. In particular, Eqs. (4) and (5) shift the optimum of the optimisation problem such that for large $B$ the optimal weights align with the red data cluster, independent of the other class. In contrast to the *discriminative explanation* of a linear classifier, which is highly task-dependent (see, e.g., first row in Fig. 2) the B-cos transform allows for a *similarity-based explanation*: a sample is confidently classified as the red class if it is aligned well with the corresponding weight vector. 

**Lastly**, these changes maintain an important property of the linear transform: similar to sequences of linear transforms, sequences of B-cos transforms can still be faithfully summarised by a single linear transform (Eq. (13)). Given the bound (Eq. (4)) and the suppression of outputs for badly aligned weights (Eq. (5)) these linear transforms will align with discriminative patterns when optimising a B-cos network for classification, see Sec. 3.2.2. As a result, these transforms are well suited to explain the model outputs.

### 3.2. Simple (convolutional) B-cos networks

In this section, we first discuss how to construct simple (convolutional) DNNs based on the B-cos transform. Then, we show how to summarise the network outputs by a single linear transform and, finally, why this transform aligns with discriminative input patterns in classification tasks. 

**B-cos networks.** The B-cos transform is designed as a drop-in replacement of the linear transform, i.e., it can be used in exactly the same way. For example, first consider a *conventional* fully connected multi-layer neural network $f(x; \theta)$ of $L$ layers, represented by

$$
f(x; \theta) = \mathbf{1}_L \circ \mathbf{1}_{L-1} \circ ... \circ \mathbf{1}_2 \circ \mathbf{1}_1(x), \tag{6}
$$

with $\mathbf{1}_j$ denoting layer $j$ with parameters $\mathbf{w}_j^k$ for neuron $k$ in layer $j$, and $\theta$ the collection of all model parameters.

![Fig. 2. Col. 2: BCE loss for different angles of $w$ for B-cos classifiers (Eq. (3)) with different values of $B$ (rows) for two classification problems. Cols. 1+3: Visualisation of the classification problems and the corresponding optimal weights (arrows) per $B$. For $B=1$ (first row) the weights $w$ represent the decision boundary of a linear classifier. Although the red cluster is the same in both cases, the optimal weight vectors differ significantly (compare within row). In contrast, for higher values of $B$ the weights converge to the same optimum in both tasks (see last row).](image)
The above discussion readily generalises to convolutional neural networks (CNNs): in CNNs, we replace the linear transforms computed by the convolutional kernels by B-cos, see Alg. 1 in supplement. Further, although we assumed a plain multi-layer network without add-ons such as skip connections, we show in Sec. 5 that the benefits of B-cos also transfer to more advanced architectures (Sec. 3.3).

3.2.1 Computing explanations for B-cos networks
As can be seen by rewriting Eq. (9), a B-cos layer effectively computes an input-dependent linear transform:

\[ l^*_j(y; W_j) = \tilde{W}_j(a_j) a_j, \tag{10} \]

with \( \tilde{W}_j(a_j) = |c(a_j; \tilde{W}_j)|^{B-1} \odot \tilde{W}_j. \tag{11} \)

Here, \( \odot \) scales the rows of the matrix to its right by the scalar entries of the vector to its left. Hence, the output of a B-cos network, see Eq. (8), is effectively calculated as

\[ f^*(x; \theta) = \tilde{W}_L(a_L)\tilde{W}_{L-1}(a_{L-1})...\tilde{W}_1(a_1 = x)x. \tag{12} \]

As multiple linear transforms in sequence can be collapsed to a single one, the output \( f^*(x; \theta) \) can be written as

\[ f^*(x; \theta) = W_{1\rightarrow L}(x)x, \tag{13} \]

with \( W_{1\rightarrow L}(x) = \prod_{l=1}^{L-1} \tilde{W}_j(a_j). \tag{14} \)

Thus, \( W_{1\rightarrow L}(x) \) faithfully summarises the network computations (Eq. (8)) by a single linear transform (Eq. (13)).

To explain an activation (e.g., the class logit), we can now either directly visualise the corresponding row in \( W_{1\rightarrow L} \), see Figs. 1 and 10, or the contributions according to \( W_{1\rightarrow L} \) coming from individual input dimensions. We use the resulting spatial contributions maps to quantitatively evaluate the explanations. In detail, the input contributions \( s^*_j(x) \) to neuron \( j \) in layer \( l \) for an input \( x \) are given by

\[ s^*_j(x) = [W_{1\rightarrow L}(x)]_{j}^T \odot x, \tag{15} \]

with \( [W_{1\rightarrow L}]_{j} \) denoting the \( j \)th row in matrix \( W_{1\rightarrow l} \); as such, the contribution from a single pixel location \((x, y)\) is given by \( \sum_{c} s^*_j(x)_{(x,y,c)} \) with \( c \) the color channels.

3.2.2 Optimising B-cos networks for classification
In the following, we discuss why the linear transforms \( W_{1\rightarrow L} \) (see Eq. (13)) can be expected to be interpretable, i.e., to align with relevant input patterns.

For this, first note that the output of each neuron—and thus of each layer—is bounded, cf. Eqs. (4) and (9). Since the output of a B-cos network is computed as a sequence of such bounded transforms, see Eq. (12), the output of the network as a whole is also bounded. Secondly, note that a B-cos network as a whole can only achieve its upper bound for a given input if the units in each layer achieve their upper bound. Importantly, as discussed in Sec. 3.1 (Eq. (4)), the individual units, in turn, can only achieve their maxima by aligning with their inputs. Hence, optimising a B-cos network to maximise its output over a set of inputs will optimise the model weights to align with those inputs.

In order to take advantage of this when optimising for classification, we train the B-cos networks with the binary cross entropy (BCE) loss

\[ L(x_i, y_i) = BCE(\sigma(f^*(x_i; \theta) + b), y_i), \tag{16} \]

for input \( x_i \) and its corresponding one-hot encoded class label \( y_i \). Here, \( \sigma \) denotes the sigmoid function, \( b \) a bias, and \( \theta \) the model parameters. In particular, we choose the BCE loss because it directly entails output maximisation. Specifically, in order to reduce the BCE loss, the network is optimised to maximise the (negative) class logit for the correct (incorrect) classes. As discussed in the previous paragraph, this will optimise the weights in each layer of the network to align with their inputs. In particular, they will need to align with class-specific input patterns such that these result in large outputs for the respective class logits.

Finally, note that increasing \( B \) allows to specifically reduce the output of badly aligned weights in each layer (cf. Eq. (4)). This will decrease the layer’s output strength and thus the output of the network as a whole for badly aligned weights, which increases the alignment pressure during optimisation (thus, higher \( B \)→higher alignment).

3.2.3 MaxOut to increase modelling capacity
As discussed in Sec. 3.2, a deep B-cos network with \( B>1 \) does not require a non-linearity between subsequent layers to model non-linear relationships. This, of course, does not mean that it could not benefit from it. While there are many potential non-linearities to choose from, in this work, we specifically explore the option of combining the B-cos transform with the MaxOut [12] operation. In particular, we model every neuron in a B-cos network by 2 B-cos transforms\(^1\) of which the maximal activation is forwarded:

\[ \text{MaxOut}(x) = \max_{i \in \{1,2\}} \{B \text{-cos}(x; w_i)\}. \tag{17} \]

We do so for two reasons. First, in order to forward a large signal, one such MaxOut unit still needs to have at least one weight vector that highly aligns with a given input and the alignment pressure is thus maintained during optimisation. Secondly, while the latter is also true for the ReLU [24] operation, we noticed that networks with the MaxOut operation were much easier to optimise. This could be due to the ‘dying neuron’ problem, cf. [12], and could potentially be remedied by better initialisation schemes.

3.3. Advanced B-cos networks
To test the generality of our approach, we evaluate how integrating the B-cos transform into commonly used DNN\(^1\)Initial experiments showed no added benefit when using more than 2 units.
architectures affects their classification performance and interpretability. In order to ‘convert’ such models to B-cos networks we proceed as follows. First, every convolutional kernel / fully connected layer is replaced by the corresponding B-cos version with two MaxOut units (see Sec. 3.2.3). Secondly, any other non-linearities (e.g., ReLU, MaxPool, etc.), as well as any batch norm layers are removed to maintain the alignment pressure and to ensure that the model can be summarised via a single linear transform.

4. Experimental setting

Datasets. We evaluate the accuracies of several B-cos networks on the CIFAR-10 [18] and the ImageNet [9] datasets. We use the same datasets for the qualitative and quantitative evaluations of the model-inherent explanations.

Models. For the CIFAR10 experiments, we develop a simple fully-convolutional B-cos DNN, consisting of 9 convolutional layers, each with a kernel size of 3, followed by a global pooling operation. We evaluate a network without additional non-linearities as well as with MaxOut units, see Sec. 3.2.3. For the ImageNet experiments, we rely on the publicly available [25] implementations of the VGG-11 [34], ResNet-32 [13], InceptionNet (v3) [39], and DenseNet-121 [14] model architectures. We adapt those architectures to B-cos networks as described in Sec. 3.3. For details on the training procedure, see supplement (Sec. C).

Image encoding. We add three additional channels and encode images as \([r, g, b, 1-r, 1-g, 1-b]\), with \(r, g, b \in [0, 1]\) the red, green, and blue color channels. On the one hand, this reduces a bias towards bright regions in the image\(^2\) [6]. On the other hand, colors with the same angle in the original encoding—i.e., \([r_1, g_1, b_1] \propto [r_2, g_2, b_2]\)—are unambiguously encoded by their angles under the new encoding. Therefore, the linear transformation \(\mathbf{W}_l \rightarrow l\) can be decoded into colors just based on the angles of each pixel, see Fig. 1. For a detailed discussion, see supplement (Sec. D).

Evaluating explanations. To compare explanations for the model decisions and evaluate their faithfulness, we employ the grid pointing game [6]. That means we evaluate the trained models on a synthetic 3x3 grid of images of different classes and for each of the corresponding class logits measure how much positive attribution an explanation method assigns to the correct location in the grid; for a visualisation of a 2x2 grid, see Fig. 3. Following [6], we construct 500 image grids from the most confidently and correctly classified images. We compare the model-inherent contribution maps, see Eq. (15), against several commonly employed post-hoc explanation methods under two settings. First, we evaluate all methods on the B-cos networks to investigate which method provides the best explanation for the same

\[\text{Evaluating models.} \quad \text{Secondly, we further evaluate the post-hoc methods on pre-trained versions of the original models (VGG, ResNet, DenseNet, InceptionNet). This allows to compare explanations between different models and to assess the explainability gain obtained by converting conventional models to B-cos networks. Lastly, all non-perturbation-based attribution maps are smoothed by a \(15 \times 15\) (3 x 3) kernel to better account for negative attributions in the localisation metric for ImageNet (CIFAR-10) images, which is negligible with respect to the overall image size.\]

Visualisation details. For generating the visualisations of the linear transforms for individual neurons \(n\) in layer \(l\) (cf. Figs. 1 and 10), we proceed as follows. First, we select all pixel locations \((x, y)\) that positively contribute to the respective activation (e.g., class logit) as computed by Eq. (15); i.e., \(\{(x, y) \text{ s.t. } \sum_c |s^{(n)}(x)|_{(x,y,c)>0}\} = c\) the 6 color channels (see image encoding). Then, we normalise the weights of each color channel such that the corresponding weights (e.g., for \(r\) and \(1-r\)) sum to 1. Note that this normalisation maintains the angle for each color channel pair (i.e., \(r\) and \(1-r\)), but produces values in the allowed range \(r, g, b \in [0, 1]\). These normalised weights can then directly be visualised as color images. The opacity of a pixel is set to \(\min(\|\mathbf{w}(x,y)\|_2/p_{99.5}, 1)\), with \(p_{99.5}\) the 99.5th percentile over the weight norms \(\|\mathbf{w}(x,y)\|_2\) across all \((x, y)\).

5. Results

In this section, we analyse the performance and interpretability of B-cos networks. For this, in Sec. 5.1 we show results of ‘simple’ B-cos networks without advanced architectural elements such as skip connections or inception modules. In this context, we investigate how the \(B\) parameter influences B-cos networks in terms of performance and interpretability. Thereafter, in Sec. 5.2, we present quantitative results of the advanced B-cos networks, i.e., B-cos networks based on common DNN architectures (Sec. 3.3). Finally, in Sec. 5.2.1, we present and qualitatively discuss explanations for outputs of individual neurons.

5.1. Simple B-cos networks

In the following, we discuss the experimental results of simple B-cos networks evaluated on the CIFAR-10 dataset.

Accuracy. In Tab. 1, we present the test accuracies of various B-cos networks trained on CIFAR-10. We show that a plain B-cos network (\(B=2\)) without any add-ons (ReLU,
Fig. 4. Col. 1: Input images. Cols. 2-6: Explanations for classes ‘horse’ and ‘car’ of models trained with increasing values of B. With higher B, the linear transforms \( W_{1 \rightarrow l} \) increasingly align with discriminative patterns and thus become more interpretable.

Fig. 5. Accuracy (crosses) and localisation (box plots) results for a B-cos network trained with different B values. While decreasing accuracy, a higher B yields significant gains in localisation.

### Tab. 1. CIFAR-10. Model accuracy of a B-cos network without any additional non-linearity (plain) and for B-cos networks with MaxOut (Sec. 3.2.3) and increasing values for B (left to right): batch norm, etc.) can achieve competitive\(^3\) performance. By modelling each neuron via 2 MaxOut units (Sec. 3.2.3), the performance can be increased and the resulting model (B=2) performs on par with a ResNet-56 (achieving 93.0\%, see [13]). Further, we see that an increase in the parameter B leads to a decline in performance from 93.8\% for B=1.25 to 92.4\% for B=2.5. Notably, despite its simple design, our strongest model with B=1.25 performs similarly to the strongest ResNet model (93.6\%) reported in [13].

### Model interpretability. As discussed in Sec. 3.2.2, we expect an increase in B to increase the alignment pressure on the weights during optimisation and thus influence the models’ optima, similar to the single unit case in Fig. 2. This is indeed what we observe. For example, in Fig. 4, we visualise \( |W_{1 \rightarrow l}(x_i)|_{W_i} \) (see Eq. (13)) for different samples \( i \) from the CIFAR-10 test set. For higher values of B, the weight alignment increases notably from piece-wise linear models (B=1) to B-cos networks with higher B (B=2.5). Importantly, this does not only lead to an increase in the visual quality of the explanations, but also to quantifiable gains in model interpretability. In particular, as we show in Fig. 5, the spatial contribution maps defined by \( W_{1 \rightarrow l}(x_i) \) (see Eq. (15)) of models with larger B values score signific-

\(^3\)A ResNet-20 achieves 91.2\% [13] under the same data augmentation.

### Tab. 2. ImageNet. Top-1 accuracy (%) for various conventional pre-trained models (pre) and their respective B-cos version.

#### Bottom row: Top-1 accuracy of a B-cos DenseNet-121 trained for more epochs and a cosine learning rate schedule (training\(^4\)).

### Classification accuracies of the pretrained [1] models and their corresponding B-cos counterparts (trained from scratch) are presented in Tab. 2. The B-cos networks (except bottom row in Tab. 2) were trained for 100 epochs with the Adam optimiser, a learning rate of \( 2.5 \times 10^{-4} \), a batch size of 256 and no weight decay. The learning rate was decreased by a factor of 10 after 60 epochs and we used RandAugment for data augmentation; for further details on training and evaluation, see supplement (Sec. C). We would like to highlight that these results are thus obtained ‘out of the box’, i.e., with a simple and commonly used optimisation scheme for all models. Thus, in spite of the drastic changes to the model architectures (no batch norm, no ReLU, no MaxPool), we are able to achieve competitive results: our B-cos VGG-11 outperforms its conventional counterpart and we only observe minor drops in accuracy w.r.t. the baseline models for the other networks, e.g., 1.1 p.p. for the DenseNet-121 (74.4\% vs. 73.3\%). By training a DenseNet-121 model for 200 epochs, a batch size of 128, learning rate warm-up and a cosine learning rate schedule, we are able to close the gap between the pretrained DenseNet-121 model and its B-cos

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counterpart (see last row in Tab. 2, ‘training’+).

**Model interpretability.** In Fig. 6, we present the explanation quality results as assessed by the localisation metric for various post-hoc attribution methods as well as the model-inherent contribution maps (Eq. (15)). We evaluated the post-hoc methods both on the conventional pretrained models (cf. Tab. 2) as well as on their corresponding B-cos counterparts; in Fig. 6, we show results for two B-cos networks, for the remaining results we kindly refer the reader to the supplement (Sec. B). In particular, we evaluated various gradient-based methods (the ‘vanilla gradient’ (Grad) [4]; Input×Gradient (IxG), cf. [2]; Integrated Gradients (IntGrad) [38]; DeepLIFT [32]; GradCam (GCam) [30]) and two perturbation-based methods (LIME [28], RISE [26]) for comparison. We would like to highlight the following two results. First, for all converted B-cos architectures, the model-inherent explanations not only outperform any post-hoc explanation for the models’ decisions, but achieve close to optimal scores on the localisation metric. Secondly, as we show in the supplement (Sec. B), none of the post-hoc methods that we evaluated for the conventional models provides a better explanation for those models than the linear transform $W_{1 \rightarrow l}(x)$ provides for the B-cos networks. Hence, by using B-cos networks instead of conventional models, it is possible to drastically improve the models’ interpretability.

For a qualitative comparison between the model-inherent explanations and post-hoc methods, see Fig. 7.

### 5.2.1 Qualitative evaluation of explanations

The following results are based on the DenseNet-121 training+ model, cf. Tab. 2: other advanced B-cos networks yield similar results, see supplement (Sec. A).

Every activation in a B-cos network is the result of a sequence of B-cos transforms. Hence, every neuron $n$ in any layer $l$ can be explained via the corresponding linear transform $[W_{1 \rightarrow l}(x)]_n$, see Eq. (13).

For example, in Fig. 1, we visualise the linear transforms of the respective class *logits* for various input images. Given the alignment pressure during optimisation, these linear transforms align with class-discriminant patterns in the input and thus actually resemble the class objects.

Similarly, in Figs. 8 and 10, we visualise explanations for intermediate neurons. Specifically, in Fig. 8, we show explanations for some of the most highly activating neurons over the validation set. We find that neurons in early layers seem to represent low-level concepts (e.g., curves), and become more complex in later layers ($l=87$: hands, $l=120$: streetcars); for additional results, see supplement Sec. A.

Fig. 10 shows additional results for neurons in layer 87. We observed that some neurons become highly specific to certain concepts, such as wheels (neuron 739), faces (neuron 797), or eyes (neuron 938). These neurons do not just learn to align with simple, fixed patterns—instead, they represent semantic concepts and are robust to changes in colour, size, and pose. Further, we found that several neurons respond preferentially to watermarks, emphasising the importance of explainability for debugging DNNs: while

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**Fig. 7.** Comparison between model-inherent explanations and the strongest post-hoc methods. More results in supplement (Sec. A.)

**Fig. 8.** Explanations for high activations of neurons from various layers. In early layers the neurons seem to encode low-level concepts (e.g., curves, see layer 38) and represent more high-level concepts in later layers (e.g., layers 87 and 120), see also Fig. 10.

**Fig. 9.** Col. 1: Input image. Cols. 2-3: Explanations for most likely classes under the model. Col. 4: Difference of contribution maps to the two class logits, i.e., $s_{c_1}^l(x) - s_{c_2}^l(x)$, see Eq. (15); positive values shown in orange ($c_1$), negative values in blue ($c_2$).
Fig. 10. Explanations of 5 individual neurons in layer 87 of a DenseNet-121. For each neuron, we provide its index number $n$ and its concept description and specificity$^4$ (left). Further, we show the 7 most activating images for each neuron (top row per neuron), in which we visualise the explanation for the highest (blue squares) activation; i.e., visualise the 72 × 72 center patch of the weighting $[W_{1→L}(X)]_n$ for neuron $n$. For some images, we additionally show the explanation for the 2nd highest activation (orange squares). Lastly, we show the explanations of the highest activations (corresponding to the blue squares) for the next 30 images to highlight the neurons’ specificity.

Unfortunately, the image is not clear enough to describe it in detail. However, it appears to show visualisations of neural activations for different neuron indices, with highlighted pixels indicating which features are most important for each neuron's activation.

5.2.2 Limitations

By normalising the weights and computing the additional down-scaling factor (see Eq. (3)), the B-cos transform adds computational overhead, which we observed to increase training and inference time by up to 60% in comparison to baseline models of the same size. However, we expect this cost to decrease significantly in the future with an optimised implementation of the B-cos transform.

Moreover, in this work we specifically investigated how to integrate the B-cos transform into CNNs for image classification. How to integrate the B-cos transform into other types of architectures, such as (vision) transformers$^{10,41}$, and how it affects model interpretability on other tasks and domains, remains an open question. Given the increasing dominance of transformers, we believe extending our method to such models to be an important next step.

6. Conclusion

We presented a novel approach for endowing deep neural networks with a high degree of inherent interpretability. In particular, we developed the B-cos transform as a modification of the linear transform to increase weight-input alignment during optimisation and showed that this can significantly increase interpretability. Importantly, the B-cos transforms can be used as a drop-in replacement for the ubiquitously used linear transforms in conventional DNNs whilst only incurring minor drops in classification accuracy. As such, our approach can increase the interpretability of a wide range of DNNs at a low cost and thus holds great potential to have a significant impact on the deep learning community. In particular, it shows that strong performance and interpretability need not be at odds. Moreover, we demonstrate that by structurally constraining how the neural networks are to solve an optimisation task—in the case of B-cos networks via alignment—allows for extracting explanations that faithfully reflect the underlying model. We believe this to be an important step on the road towards interpretable deep learning, which is an essential ingredient for building trust in DNN-based decisions, specifically in safety-critical situations.

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$^4$We manually evaluated the first 100 images for each neuron and found the respective neurons to reliably highlight the assigned concept, i.e., their linear explanations $[W_{1→L}(X)]_n$ are similar to those shown in Fig. 10.
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