Distributed Fiber Optical Technology for Damage Identification of Engineering Structure

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Xiaoma Dong, Liqiang Zhou
ZheJiang Industry Polytechnic College, ShaoXing, China
dxmlz201123@21cn.com

Abstract—To conduct optical fiber monitoring rock slide model test and optical fiber monitoring of steel concrete interface slip model test, the large tri-axial shear test of geotechnical engineering was used. First, the data of sliding distance and optical loss and their dynamic range were obtained. Second, the slide distance and fiber loss relation curve and the fitting equation were worked out. Finally, the typical applications of optical fiber sensing technology in Rock Engineering (high slope engineering, rock foundation of Dam Engineering) slope stability and geological disaster monitoring were put forward. The results showed that optical fiber sensing was very sensitive, and the loss value was 30 to 50dB. The dynamic range of rock slide monitoring fiber was 3 to 3.5mm, and the dynamic range of the interface slip monitoring fiber was 1.6mm. Thus, the sensing system can detect the sliding process of the interface between the concrete and the steel plate. It provides some reference for the sliding monitoring of the composite materials.

Keywords—Optical fiber sensing technology; sliding distance-fiber loss; engineering structure damage

1 Introduction

Structural fracture damage occurs mostly inside the component, which is generally difficult to be observed by the naked eye. The damage caused by the reduction of stiffness is partial, macro feature structures (such as deformation etc.) or function did not change significantly in the general case, when the damage extended to a certain extent it will trigger sudden catastrophic events, causing major losses. The damage identification of such problem in the internal structure is a hard nut to crack. In addition, the accidents of high slope landslide and rock slip and the steel-concrete composite structure are applied more and more widely in modern large-scale civil engineering. The main form of failure is the interface slip between steel and concrete. How to monitor the internal sliding damage of this type is a new problem facing damage identification.

Therefore, how to use non-destructive detection methods to detect these hidden problems effectively, especially in real-time, has increasingly become a research topic in the field of civil engineering and other engineering fields. Its significance is self-
evident. The study of the related identification methods will play a key role in improving the reliability and safety of the structure. In addition, internal damage detection for important and old buildings, such as large bridges and workshops, and reinforcement and prolongation of service life based on test results are also a concern for civil engineering sector.

2 State of the art

The basic idea of damage identification in engineering structure is as follows. When the structure is damaged, the stiffness and bearing capacity of the corresponding parts decrease, which leads to the change of the dynamic characteristics of the structure. Chapeleau X et al. [1] applied the distributed optical fiber sensing technology to the pavement crack detection. By comparing the vibration information of undamaged structure and damage structure, the location of damage and the degree of damage are determined. Using the distributed optical fiber sensing technology, Piao, C. et al. [2] detected the abnormality of the grouting shaft wall. The basic process is as follows. The finite element modeling and finite element modal analysis are carried out for the original design of the structure. Rajan, G. et al. [3] used optical fiber sensing technology to evaluate the physical properties of dental resin composites. The modal and frequency of the structure are predicted as the dynamic information under the undamaged state of the structure. The experimental modal analysis is carried out on the actual structure with damage, and the modal parameters are obtained as the information to be checked. Based on distributed optical fiber sensing technology, Giannoccaro, N. I. [4] used a new tactile optical device to detect small incision damage. The structural dynamic characteristics obtained from the test were compared with those predicted by mathematical models, and the location and degree of damage were determined. The numerical simulation method is usually combined with the dynamic test. Su, H. et al. [5] pointed out that the integrity and safety of dike projects are objectively undermined by crossing culverts and other hydraulic structures, especially earth-rock junctions.

An optical fiber system (includes an optical fiber communication system or an optical fiber sensing system), consists of three basic components: light source, optical fiber, photodetector. There are two kinds of light source: semiconductor laser (LD) and semiconductor light emitting tube (LED). The former is more common, that is, the laser signal is commonly used in the light source. The laser frequency is single (monochromatic), the directivity is good, and the intensity is high. There are two main types of laser emission: pulse type and continuous type. When fiber is used for signal transmission, fiber is usually used in the form of fiber cable, that is, multi fiber cluster formed optical cable. Multiple cables are loaded into a loose tube (plastic pipe) and become a cable unit. A number of loose sleeves are made into a bundle, and a sheath is combined to form a fiber optic cable. Its center is metal or nonmetal reinforcement (such as steel strand) to strengthen the mechanical strength and bearing capacity of the optical fiber cable. In order to enhance its waterproof and moisture-proof ability
and prolong the service life (more than 20 years), the waterproof ointment of the cable core can be filled between the loose sleeves.

Optical detector (optical detector) is the terminal of optical fiber system. It is an optical signal receiving device. It is an active device that transforms the optical signal into the electrical signal. Optical detection of optical fiber system adopts photon detector. The principle is to transform photon energy into electric field and current by means of semiconductor with specific structure, and its quantum efficiency is 80~90%. Barrias, A. et al. [6] found that the singular area of internal temperature in buildings would not be detected inevitably because of a large layout spacing of thermistor thermometers and other reasons. Fiber optic sensing is developed with the development of optical communication and the development of IT industry. Many of the devices of optical fiber sensing are common to optical communication in order to reduce the cost by using the advantage of batch quantization. In optical fiber sensing, sensing optical fiber directly transforms environmental signals—monitoring and measuring (such as temperature) into optical signals, that is, optical waveguides in sensing fibers directly accept the modulation of environmental physical quantities.

Masoudi and Newson [7] pointed out that the distributed optical fiber sensing is a unique sensing technology that traditional electric sensing technology does not have. It can measure the physical field along fiber laying path. Lim, K. et al. [8] used a distributed optical fiber sensor to monitor the pressure and stiffness changes in the tube. In recent years, a large number of studies have been carried out to detect the condition of large buildings, dams, bridges and other structures with distributed optical fiber sensing. It is possible to monitor the sliding of the rock mass by embedding the borehole or backfilling cement mortar into the rock mass. Tejedor, J. et al. [9] proposed a machine learning method for pipeline monitoring system based on distributed acoustic sensing. Before sliding, the loss curve detected by OTDR is basically flat. Once sliding occurs, the fiber embedded in the rock will bend and form loss. Lomotowski, G. and Bereś-Pawlik, E. [10] pointed out that due to the loss caused by sliding, the backscatter signal detected by OTDR has a sudden drop. Therefore, the width of the slide can be determined according to the size of the loss, and the position of the slide can be determined by the location of the loss point on the optical fiber. Distributed optical fiber sensing and monitoring technology are able to get the continuous distribution of measured information in space and time. It is very suitable for condition monitoring of complex structure such as linear submarine pipeline, oil well and large civil engineering structure.

To sum up, the traditional method cannot monitor the hidden problem of internal sliding damage in civil engineering. To solve this problem, the large triaxial shear test of geotechnical engineering was used. First, the data of sliding distance and optical loss and their dynamic range were obtained. Second, the slide distance and fiber loss relation curve and the fitting equation were worked out. Finally, the typical applications of optical fiber sensing technology in Rock Engineering (high slope engineering, rock foundation of Dam Engineering) slope stability and geo-logical disaster monitoring were put forward. The sensing system can detect the sliding process of the interface between the concrete and the steel plate. It provides some reference for the sliding monitoring of the composite materials.
3 Optical fiber micro bending loss sensing principle

3.1 The light guiding principle of optical fiber

Modern physics believes that the nature of light is the "two wave particle dualism", namely, in different conditions it either fluctuates or shows corpuscular property, when it fluctuates, we call it optic wave and when it demonstrates the latter property, we call it photon beam. Light is mainly manifested in optic wave. It can be described by Maxwell’s electromagnetic wave equation. When light is emitted and is interacting with other substances, light shows particle property and follows quantum theory. According to the wave optics, light is an electromagnetic wave.

One of the basic principles of light conduction is that the properties of light in different optical media (velocity, direction) change accordingly. The conduction velocity of light in the vacuum is 300 thousand km/s, and the velocity is reduced when it is conducted through other media. The degree of slowing down the speed of light in a medium is expressed by the refractive index of the medium, that is, as shown in (1).

\[ n = \frac{c}{v} \]  

In the formula, \( n \) is the refractive index, \( c \) is the vacuum speed (km/s) and \( v \) is the speed of light, the medium (km/s).

3.2 Light loss

Total reflection creates the basic condition for light transmitting in long distance through optical fiber. The basic structure of optical fiber can restrain the light injected into the optical fiber in the optical fiber, and avoid the loss of optical power at the core cladding interface. However, there are two other reasons that lead to the loss of light power in the process of light conduction, which decreases with the increase of the conduction distance and it is called light attenuation or loss. The transmission loss of optical fiber includes two kinds of intrinsic loss and non-intrinsic loss. The intrinsic loss of the material is caused by the intrinsic properties of the material, which is not related to the external environment. The source of the intrinsic loss includes: material absorption and material scattering.

The distributed optical fiber sliding sensor is based on the Rayleigh scattering loss of [160 ~ 162]. Rayleigh scattering loss is caused by the non-directional conduction of light in the optical fiber. The scattering loss includes 3 types: Rayleigh (Rayleigh) scattering; Raman (Raman) scattering; Brillouin (Brillouin) scattering.

Although the optical fiber manufacturing process has reached an almost perfect degree, the fiber material still exists inhomogeneity on the microcosmic (less than light wavelength or molecular weight). For light waves, this inhomogeneity is the microscopic aberration of refractive index, resulting in the non-directional scattering of light, that is, a small part of light will be converted into scattered light, including forward scattered light and backscattered light, as shown in Figure 1. The latter has an important special significance for optical fiber sensing.
Rayleigh scattering is the most important scattering, and Rayleigh scattering loss plays an important role in the total optical fiber loss. The basic characteristics of Rayleigh scattering light: the frequency and wavelength of Rayleigh scattering light are the same as those of the optical waveguide; the light power of Rayleigh scattering light is proportional to the 4th power of the wavelength.

The position of the scattering point can be determined by accurately measuring the time interval of the incident time of the incident light pulse to the backscattered light, as shown in formula (2):

$$x = v \cdot t/2$$

(2)

This is the principle of the optical radar. In formula (2), X is the light path of the scattering point to the optical fiber entrance.

### 3.3 Distributed optical fiber slide sensing technique

The principle of optical fiber sensing is that environmental factors acting on optical fiber will affect the transmission of optical waveguides in the optical fiber, and we can perceive environmental parameters by detecting the change of optical waveguides. The distributed optical fiber sensing of rock mass sliding can detect the continuous distribution of random cracks. The optical fiber crack sensing method is the intensity modulated optical time domain method modelled on the micro bending mechanism. The detected optical information carrier is Rayleigh scattering. It belongs to intrinsic scattering and exists everywhere in the core, thus providing optical information along the whole fiber.

When a laser pulse is incident on a single-mode fiber, the backward light of Rayleigh scattering is received by the optical time domain reflector (OTDR) at the entrance. The control equation of optical power is shown in Formula 3.
In the formula, $P(x)$ is the backward light power, $X$ is the distance along the optical fiber, $S(x)$ is the scattering acquisition ratio, the $\alpha_s$ is the scattering coefficient, $V_g$ is the optical group velocity in the optical fiber, and $\alpha_f$ and $\alpha_b$ are forward and backward attenuation coefficients respectively. OTDR is the optical radar, and there is a simple correlation between the distance $X$ and the positive and reverse transmitting time of light, as in the formula (4):

$$X = \frac{1}{2} t V_g$$

Normally, for the same fiber, we have $\alpha_f = \alpha_b = \alpha$ and $S$ is a fixed value, light loss value grows exponentially, as shown in formula (5):

$$P(x) = A \alpha_s \exp(-2\alpha x)$$

$A$ is a constant. Although the value of $\alpha$ generally changes with the value of $\alpha_s$, the integral $\int_0^x \alpha(x') \, dx'$ is still very small and its error is very small.

The sliding of the rock layer causes the micro bend of fiber buried under, increasing the loss; the change of the light power is detected by the OTDR and is located. The basic optical layout and light attenuation waveforms of the distributed optical fiber sliding sensing with OTDR are used in Figure 2.

![Optical path layout and attenuation curves of sliding optical fiber sensing in rock mass](http://www.i-joe.org)
Distributed optical fiber sliding sensing is based on single mode optical fiber. When embedded in, it is arranged diagonally or orthogonally with the possible sliding rock layer. Once the level slipped, the fiber will bend slightly. As a sensing mechanism, the light loss is aggravated by the micro bending, and the back light is used as the information carrier, and it is perceived and located by OTDR.

The distributed optical fiber sliding sensing system consists of sensing optical fiber, transmission optical cable, passive device, optical demodulator, PC, and special software.

4 Distributed optical fiber sensing sliding model test

4.1 Tools for the experiment

In order to simulate the complex deformation state of the actual sliding structure, the triaxial compression experiment is adopted. This ensures that the sensing fiber in the whole process is in a state of embedment, and it is close to the actual structure to the maximum extent. The experiment machine is a SZ-40 type large triaxial compressor, which can add the maximum confining pressure of 2.5MPa and the maximum compression stroke of 60mm. Before the experiment, the optical fiber is first used to detect each fiber by fiber optic conductance. In experiment, we use optical power meter to observe the loss of Al9201A type observation fiber, in order to observe the relationship between the change of optical fiber loss and the sliding displacement.

4.2 Experiment methods

The confining pressure of the triaxis test is uses $\sigma_2 = \sigma_3$. The specimen is a cylindrical concrete structure, and the design strength is C40. In the cylindrical specimens of the upper and lower circular section pressure induced crack to structure along the direction of slip, so as to realize the monitoring of optical fiber sensing sliding induced by sliding plane when sliding, trying to find changes in fiber loss in a slip failure process.

When preparing the specimen, considering that the optical fiber is damaged, 5 parallel and continuous optical fiber distributed layout modes are adopted, and the optical fiber also adopts different diameter sizes, namely, 2 of 900µm, 2 of 600µm and another one, 250µm. The induction seam is uses the organic glass sheet. In the concrete pouring, the lubricating oil is applied to the upper and lower surfaces of the sheet in order to achieve the effect of sliding along the induced seam. A circular tube made of $\phi$ 160mmPVC is used as the test mold. The optical fiber is fixed in fine iron wire in the pipe, and the adhesive is applied to the contact point between the optical fiber and the wire, so as to minimize the bending loss of the optical fiber. The residual fiber at the bottom of the circular pipe is surrounded by a circular way, and then drawn from the special protective hole of the induced slot. The optical fiber is not contacted with the tube wall, and there should be no micro bending effect in the pipe. 2 specimen
pieces are made, so 2 PVC tubes prepared, also 2 groups of sensing fibers (5 for each

When the fiber is arranged in the PVC tube, the concrete is poured after the pass is

Table 1. Sensing fiber number table

| Number | 1     | 2     | 3     | 4     | 5     |
|--------|-------|-------|-------|-------|-------|
| Fiber optic parameter | φ900µm | φ900µm | φ600µm | φ600µm | φ250µm |

Table 2. Specimens with the ratio parameters

| Parameters         | Water cement ratio | Per unit water use | Sand content | Concrete proportion (volumetric method) |
|--------------------|--------------------|--------------------|--------------|----------------------------------------|
| Concrete parameter | 0.41               | 190                | 33%          | Cc: Sc: Gc: Wc=1.0:1.64:3.41:0.52         |

4.3 **Test on the model**

When the fiber is arranged in the PVC tube, the concrete is poured after the pass is

The triaxial compression test process was carried out after 28 days of maintenance. The test steps are as following:

The peripheral coarse aggregate used in the experiments is screened (the maximum particle size of not more than 20mm). At the same time, the final check before the fiber test is carried out.

The whole specimen is loaded with rubber film to protect the whole inner wall of the triaxial instrument.
The fiber is extracted from the specimen into the upper pressure discus, and is wrapped up in plastic hose to avoid damage.

The optical fiber is wrapped in a plastic tube and then penetrated into the drainage hole of the base of the triaxial instrument.

Wrap the coarse aggregate with a wire cage around the specimen.

And then operate according to the triaxial test procedure, specifics are omitted.

Add pressure and operate according to the triaxial test regulations, see The Rock Test Regulations of Water Conservancy and Hydropower Projects.

4.4 Fiber loss monitoring and statistics analysis

After installing the specimen according to the triaxial experimental procedure, we first conduct a fiber optic conductivity detection. It is found that the 250µm optical fiber of the 1 specimen is damaged during the installation. It is also found that the No. 4 fiber of the 2 specimen is broken and the rest of the fiber is intact. The loss observation is based on the AI9201A type of optical power meter. In order to facilitate observation, we should reduce the step length during the test so as to observe the relationship between the power loss in the process of specimen failure and find out the law for the change.

When the specimen is installed in the triaxial instrument and the final passage is detected, the 600µm fiber of the 1 specimen is founded damaged in the installation.

The slip causes the fiber to produce two micro bends. Considering that there are only two sets of power meters in the optical fiber observation, 2 perfect fibers are selected for loss detection. When the loss of fiber is observed, the pressure step should be minimized. The loss changes are recorded on time during the observation.

It is found that the attenuation of optical fiber power is very sensitive to the slip deformation of the structure. Before the axial compression begins, the attenuation increases with the increase of the slip distance.

During the triaxial compression test of No. 1, because the weight of gravel around the specimen pulled down the rubber membrane, resulting in the closed confining pressure. This led to ambient pressure leakage 10 minutes after the start of the test, that is, the ambient pressure water was emitted from the optical fiber through the hole (drainage hole), and it had a certain initial speed from the flow rate of the water, which was considered to be the ambient pressure leakage. At the same time, the pressure gauge also shows that the confining pressure output is zero, so it is considered that the test piece 1 is a uniaxial compression test without confining pressure.

As can be seen from figures 3 and 4, the attenuation curve is more regular. With the increase of the sliding distance, the attenuation increases gradually. Then the loss is dramatically changed, and the fiber is cut when the skid distance is 3.5 to 4.0mm.
A semi empirical formula for calculating the attenuation value is presented on the basis of the relationship between the observed data and the variation of the measured data between the slip distance and the loss.

\[
A(\Delta l) = -\beta \frac{l}{g} \theta (\Delta l)^{\xi_{\text{sin}} \theta}
\]  

(6)
In the formula, $\beta_1$ and $\beta_2$ are constant, $\Delta l$ as the sliding distance (the unit is mm), $\theta$ as the included angle between the sliding surface (if it is a circular arc then take the tangent point that suggests the sliding trend) of fiber and rock (usually obtuse angle).

The $-\beta_1 \tan \theta$ in formula (6) is the contribution of the shearing to light attenuation, and $\frac{\beta_2}{\sin \theta}$ is the contribution of the tensile effect to the light attenuation. When the parameter $\theta$ is small, the shear force is the influence that affects the sliding rock mass, the value of $-\beta_1 \tan \theta$ is thus bigger; when $\theta$ is larger, tensile force of fiber mainly affects the sliding rock by the sliding force exerted, so the $-\beta_1 \tan \theta$ value is larger. The observed attenuation values are results of joint action of the shearing and tensile force.

The coefficient $\beta_1$ and $\beta_2$ in the formula (6) can be obtained by the least square method. If Figure 3 and 4 are introduced to the formula (6) and starts the least square fitting. After fitting the sensing data of 2 sliding optical fibers, we can draw a conclusion that the coefficient $\beta_1$ and $\beta_2$ are close to each other. We can get the data fitting of $\beta_1$ and $\beta_2$ in pairs using formula (6) in several groups of experiments, and get the values of multiple groups of $\beta_1$ and $\beta_2$ respectively, and then we can get the average value. By calculating these values produced thereof, we can have the correlation between light loss $A$ and sliding distance $\Delta l$ and between $A$ and $\theta$, the included angle, the ideal model will thus be obtained.

5 Distributed optical fiber sensing interface slip monitoring model test

The application of steel-concrete composite bridge panel is becoming more popular. This is thanks to the bonding performance safety and durability of the structures with steel concrete interaction and steel-concrete interface. Therefore, it is of practical significance to monitoring the interface slip damage. This paper tested the steel-concrete interface slip using the distributed optical fiber sensing. The equipment used in the test, the test process and the concrete specimen pouring are the same as that of the previous rock mass sliding monitoring model test.

5.1 Experiment method

In order to simulate the sliding of the steel-concrete interface. The specimen is embedded in the concrete with a steel sheet (about 3mm), and the direction of the steel plate and the concrete slip is roughly parallel. The fiber is arranged on the surface of the steel plate and is tightly attached to the steel plate. At this point, the micro bending loss of the fiber reflects the sliding process of the interface between the upper concrete and the steel plate.

5.2 Choose the type of fiber optic and laying methods

Two parallel optical fibers (1# $= -900\mu m$, 2# $= -600\mu m$) are used in the selection of optical fiber specimen. The combination of epoxy resin, curing agent and aluminum oxide powder is used to paste. To make sure it is fast bound together, the fiber is pressed close with fine wire. See Figure 5 and Figure 6.
5.3 Experiment results

A total of 2 specimens were prepared. One is not tested due to the inferior conductivity of its monitoring interface. The observation is given up. The interface sliding test of No. 1 fiber in another specimen is shown in Figure 7.
In bridge and other engineering, steel plate concrete composite structure is applied widely, the problem of steel plate concrete fastness directly relates to the lifespan of the structure. The optical fiber sensor can be embedded in the steel concrete interface to monitor the slip state.

6 Conclusion

On the basis of the analysis of mechanics and optics principle of optical fiber sensing, distributed optical fiber slide sensing and interface slip sensing technology are put forward, which can be used for rock slide and steel-concrete interface slip monitoring. Through this study, the following conclusions are drawn.

(1) The triaxial model tests of optical fiber slide sensing and optical fiber interface slip have been carried out. The data of the corresponding relation between the slip and the loss of light are obtained. It showed a regular change; the measurement value is reasonable and credible.

(2) The structure shows that optical fiber sensing is very sensitive, and the loss value is 30 to 50dB. The dynamic range of rock slide monitoring fiber is 3 to 3.5mm, and the dynamic range of the interface slip monitoring fiber is 1.6mm.

(3) The bonding process of the fiber is carried out by the combination of epoxy resin, curing agent and aluminum powder. The experiment shows that the sensing system can detect the sliding process of the interface between the concrete and the steel plate. It provides some reference for the sliding monitoring of the composite materials.
7 References

[1] Chapeleau X, Blanc J, Hornych P, et al. Assessment of cracks detection in pavement by a distributed fiber optic sensing technology. Journal of Civil Structural Health Monitoring, 2017, vol. 7(2), pp. 1-12.

[2] Piao, C., Yuan, J., Shi, B., Lu, H., Wei, G., & Gu, C. Application of distributed optical fiber sensing technology in the anomaly detection of shaft lining in grouting. Journal of Sensors, 2015, vol. 1, pp. 1-8.

[3] Rajan, G., Shouha, P., Ellakwa, A., Bhowmik, K., Xi, J., & Prusty, G. Evaluation of the physical properties of dental resin composites using optical fiber sensing technology. Dental Materials, 2016, vol. 32(9), pp. 1113-1123. https://doi.org/10.1016/j.dental.2016.06.015

[4] Giannoccaro, N. I., Massaro, A., Spedicato, L., & Lay-Ekuakille, A. Detection analysis of small notches damages using a new tactile optical device. IEEE/ASME Transactions on Mechatronics, 2015, vol. 20(1), pp. 313-320. https://doi.org/10.1109/TMECH.2014.2301638

[5] Su, H., Yang, M., Zhao, K., & Wen, Z. Blind source separation model of earth-rock junctions in dike engineering based on distributed optical fiber sensing technology. Journal of Sensors, 2015, pp. 1-6. https://doi.org/10.1155/2015/281538

[6] Barrias, A., Casas, J. R., & Villalba, S. A review of distributed optical fiber sensors for civil engineering applications. Sensors, 2016, vol. 16(5), pp. 748. https://doi.org/10.3390/s16050748

[7] Masoudi, A., & Newson, T. P. Contributed review: distributed optical fibre dynamic strain sensing. Review of Scientific Instruments, 2016, vol. 87(1), pp. 111-112. https://doi.org/10.1063/1.4939482

[8] Lim, K., Wong, L., Chiu, W. K., & Kodikara, J. Distributed fiber optic sensors for monitoring pressure and stiffness changes in out-of-round pipes. Structural Control and Health Monitoring, 2016, vol. 23(2), pp. 303-314. https://doi.org/10.1002/stc.1771

[9] Tejedor, J., Macias-Guarasa, J., Martins, H. F., Pastor-Grabels, J., Corredera, P., & Martin-Lopez, S. Machine Learning Methods for Pipeline Surveillance Systems Based on Distributed Acoustic Sensing: A Review. Applied Sciences, 2017, vol. 7(8), pp. 841. https://doi.org/10.3390/app7080841

[10] Lomotowski, G., & Bere-Pawlak, E. A method of measuring moving element displacements in micro-hydraulic valves with the use of optical fibers. Journal of Theoretical and Applied Mechanics, 2014, vol. 52(3), pp. 781-791.

8 Authors

Xiaoma Dong and Liqiang Zhou are with ZheJiang Industry Polytechnic College, ShaoXing, 312000, China.

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