Sharing but not caring: dark matter and the baryon asymmetry of the universe

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Abstract. We consider scenarios where Dark Matter (DM) particles carry baryon and/or lepton numbers, which can be defined if there exist operators connecting the dark to the visible sector. As a result, the DM fields become intimately linked to the Standard Model (SM) ones and can be maximally asymmetric just like the ordinary matter. In particular, we discuss minimal scenarios where the DM is a complex scalar or a Dirac fermion coupled to operators with nonzero baryon and/or lepton numbers, and that consist of only SM fields. We consider an initial asymmetry stored in either the SM or the DM sector; the main role of these operators is to properly share the asymmetry between the two sectors, in accordance with observations. After the chemical decoupling, the DM and SM sectors do not care about each other as there is only an ineffective communication between them. Once the DM mass is specified, the Wilson coefficients of these operators are fixed by the requirement of the correct transfer of the asymmetry. We study the phenomenology of this framework at colliders, direct detection and indirect detection experiments. In particular, the LHC phenomenology is very rich and can be tested in different channels such as the two same-sign leptons with two jets, monojet and monojet with a monolepton.

Keywords: baryon asymmetry, dark matter theory, particle physics - cosmology connection

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1 Introduction

While there is no evidence of the presence of primordial antimatter in the universe, the amount of primordial matter, i.e. baryons, has been determined quite precisely from two independent observables. From the measurements of the primordial deuterium abundance of the Big Bang Nucleosynthesis (BBN) and the temperature anisotropies in the Cosmic Microwave Background (CMB), the amount of baryons as a fraction of cosmic critical energy density is determined to be $\Omega_{\text{BBN}}^{\text{B}} = 0.048 \pm 0.002$ [1] and $\Omega_{\text{CMB}}^{\text{B}} = 0.048 \pm 0.001$ [2], respectively. In addition, the CMB measurement also yields the amount of nonbaryonic matter, i.e. the so-called Dark Matter (DM), to be $\Omega_X = 0.258 \pm 0.008$ [2]. Given that the evidences of DM arise only from gravitational effects, it could be some form of exotic matter or a particle very similar to its baryonic counterpart, in particular it could be asymmetric. The simplest asymmetric DM is either a complex scalar $\phi$ or a Dirac fermion $\psi$ uncharged under the SM gauge group. A single Weyl fermion is not a suitable candidate since it would be either massless or have a Majorana mass, meaning that it cannot carry an asymmetry. The idea of an asymmetric DM giving rise to comparable DM and baryon densities is a few decades old [3–5]. In recent years, this idea has received a renew impetus and a plethora of the new ideas culminate in some recent review articles [16–19] (see also [20–22]). Just like in a baryogenesis scenario, when Sakharov’s conditions [23] are fulfilled, one could dynamically generate an asymmetry in $X \equiv \{\phi, \psi\}$. One can take this one step further and expect that like in the Standard Model

1 The connection between DM and the baryon asymmetry has also been explored in the context of symmetric DM (See e.g. refs. [6–15]).
(SM), there are additional fast interactions among the DM sector which efficiently annihilate away the symmetric component \((XX \rightarrow \cdots)\), ending up with only the asymmetric part.

Up to now there is no compelling evidence that DM communicates with the SM via interactions other than gravity; and if this is all that is, the possibilities of testing DM properties in the lab are very challenging. On the other hand, there are hints of a deeper connection between DM and the SM baryons. For instance, their energy densities today are of similar order, which would suggest a common mechanism for the origin of the two species: 

\[
    r \equiv \frac{\Omega_X}{\Omega_B} = \frac{Y^0_X m_X}{Y^0_{BSM} m_n} = \frac{|Y_{\Delta X}| m_X}{Y_{\Delta BSM} m_n} = 5.4,
\]

where \(m_X\) and \(m_n\) are the DM and the nucleon mass, respectively. Here we denote \(Y_{\Delta i} \equiv Y_i - Y_i^0\), where \(Y_i = n_i/s\) is the number density of \(i\) normalized by the entropic density \(s = \frac{2e^2}{45} g_* T^3\), \(g_*\) is the relativistic degrees of freedom that contribute to the entropy and \(T\) the temperature of the thermal bath. In eq. (1.1), the superscript ‘0’ denotes the value today, \(Y^{0}_{BSM} = (8.66 \pm 0.09) \times 10^{-11}\) [2] and the third equality is due to the assumption that both DM and baryon are maximally asymmetric.\(^2\) We also denote \(Y^{0}_X = |Y_{\Delta X}|\) because DM today can consist of particles \(X\) or antiparticles \(X\). Notice that the asymmetric DM scenario itself does not justify why \(r \sim 1\); further theoretical inputs which relate \(m_X\) to \(m_n\) or \(Y_{\Delta X}\) to \(Y_{\Delta BSM}\) are needed (see e.g. ref. [25–28]).

In this work, we are not trying to dynamically generate \(r \sim 1\), but we will rather take it as a starting point. Our aim is to consider an Effective Field Theory (EFT) description where the DM and the SM sectors share a common asymmetry via interactions that were typically in equilibrium. After the chemical decoupling between the two sectors, they barely interact i.e. not caring about each other. In particular, we consider an asymmetric DM scenario in which the DM is not charged under the SM gauge symmetry,\(^3\) which makes its detection particularly challenging through SM interactions. We further assume that the DM particles do carry nonzero lepton and/or baryon number [32–44]\(^4\) which is fixed by their coupling to the SM fields through higher dimensional operators of the form

\[
    \frac{1}{\Lambda^{2-p/2}N+n-4} X^N \mathcal{O}_{SM}^{(n)}, \tag{1.2}
\]

where \(\Lambda \equiv \Lambda'/\lambda\) with \(\Lambda'\) being the effective scale below which the effective operators are valid and \(\lambda\) the coupling constant between the DM and the SM sectors. \(\mathcal{O}_{SM}^{(n)}\) is a SM gauge invariant operator of dimension \(n\) consisting of only SM fields and \(p = 1, 2\) for \(X\) being a fermion or a scalar, respectively. To ensure the stability of DM particles, one needs \(N \geq 2\), which can be due to specific baryonic and/or leptonic charges carried by the DM. In this work, we consider the minimal scenario with \(N = 2\), where these higher dimensional operators play the crucial role of distributing the asymmetry between the SM and the DM sectors. As it will be shown, this scenario is predictive since there is only a limited number of possible higher dimensional operators that can be written down; for a given DM mass, their Wilson coefficients are fixed by the requirement that the asymmetry between the SM and the DM sectors is correctly distributed to match the observations.

\(^2\)Ref. [24] considered both the symmetric and the asymmetric DM components.

\(^3\)DM candidates can also be the lightest neutral components of some SU(2)\(_L\) multiplets (with zero or nonzero hypercharge). The quest to find such particles which are automatically stable was carried out in ref. [29]. Asymmetric DM from SU(2)\(_L\) multiplets with nonzero hypercharge were considered in refs. [30, 31].

\(^4\)For DM realizations within baryon and lepton number as gauge symmetries see e.g. refs. [45–48].
The mass of the DM particles can span a wide range, from few GeV up to $\sim 100$ TeV. If $X$ carries nonzero baryon number, we have to restrict $2m_X \gtrsim m_n$ to prevent fast nucleon decays. Requiring all the DM symmetric component to be annihilated away, the upper bound ($m_X \lesssim 100$ TeV) has to be imposed in order to avoid unitarity violation [49, 50]. The heavier the DM particles are, the more nonrelativistic they have to be during chemical decoupling. This happens because it is necessary to suppress their asymmetry density through a Boltzmann suppression factor to obtain the correct relic abundance (see e.g. ref. [51]).

In the sharing scenario, we assume a net nonzero charge asymmetry is generated at some high scale. Since the sharing operator (1.2) does not violate the charge, its role is to distribute the asymmetry among the dark and visible sectors. Figure 1 illustrates the sharing mechanism for the cases where the dark and visible sectors get into chemical equilibrium or not. In the case where the system achieves chemical equilibrium (left panel), both asymmetries depend on the same chemical potential ($\mu$). If the DM is nonrelativistic when the two sectors decouple at $T = T_f$, a Boltzmann factor suppresses its number asymmetry. On the other hand, for the scenario in which the system never reaches the chemical equilibrium (right panel), the sector where the initial asymmetry resides does matter, and the asymmetries in the dark and the SM sectors are characterized by the chemical potentials $\mu_X$ and $\mu_{SM}$, respectively. For instance, if the initial total asymmetry is stored in the dark sector, the amount of asymmetry transferred to the SM depends on the strength of the coupling between these two sectors, which is represented in figure 1 by $1/\Lambda$.

The present work is complementary to previous studies in the following ways: i) our discussion is model-independent: we write down all possible effective operators and focus on the lowest dimensional ones; ii) we cover the whole DM mass range where the effective operator description is valid; iii) we determine the viable parameter space taking into account various phenomenological constraints. Note that our study does not apply for the cases where the effective operator description is not valid such as the scenario proposed in ref. [53] where the mediator which links the SM and DM sectors is light, with a mass comparable to the DM one.

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5This is in contrast to scenarios which consider a net zero asymmetry where the dark and visible sectors carry an equal but opposite sign asymmetry e.g. ref. [52].
The paper is organized as follows: in section 2 we introduce the generalities of the model where DM particles carry baryon and/or lepton number. In section 3, we discuss in detail the transfer of the asymmetry, whether it is effective before or after the freeze out of the electroweak (EW) sphaleron processes. A number of phenomenological constraints and future detection prospects are discussed in section 4: DM direct and indirect detection, and the bounds coming from the Large Hadron Collider (LHC). Concluding remarks are presented in section 5.

2 Baryonic and leptonic dark matter

In order to connect the DM and the SM sectors, our working assumption is that the DM particles carry baryon $B$ and/or lepton $L$ numbers. Of course, one could only define these quantum numbers if there exist operators which relate the DM and the SM baryons and/or leptons. In particular, we consider minimal models in the sense that the DM particles are singlets under the SM gauge group and they are either complex scalars or Dirac fermions. We consider that they couple in pairs ($N = 2$) to the SM, so that the operator (1.2) reduces to

$$\frac{1}{\Lambda^{n-p}} X X \mathcal{O}^{(n)}_{\text{SM}}.$$ 

(2.1)

To make sure that the effective operator description remains valid, we require $\Lambda' = \lambda \Lambda \gg E$, where $E$ is the characteristic energy scale being probed. Taking the largest coupling before perturbative expansion breaks down i.e. $\lambda = 4\pi$, we have $\Lambda \gg E/(4\pi)$; however, one should keep in mind that the description could also break down earlier, for $\lambda < 4\pi$. As we will see in more detail later, for the scenario after EW symmetry breaking, we also impose $\Lambda > v$, where $v = \langle H \rangle = 174$ GeV is the Higgs vacuum expectation value (vev) such that this framework remains consistent.

Notice that part of our minimality criteria is to assume that $\mathcal{O}^{(n)}_{\text{SM}}$ does not contain new fields beyond the SM. We further assume that the operator (2.1) preserves $B$ and $L$, which implies that $B(X) = B \left( \mathcal{O}^{(n)}_{\text{SM}} \right) / 2$ and $L(X) = L \left( \mathcal{O}^{(n)}_{\text{SM}} \right) / 2$. Assuming that the total asymmetry in a charge $q$ is preserved, the operator (2.1) plays a role in distributing the asymmetry among the DM and the SM sectors with

$$Y_{\Delta q} \equiv q_X Y_{\Delta X} + Y_{\Delta q_{\text{SM}}} = \text{constant} \neq 0,$$  

(2.2)

where $Y_{\Delta q_{\text{SM}}} = \sum_{\Psi_{\text{SM}}} q_{\Psi_{\text{SM}}} Y_{\Delta \Psi_{\text{SM}}}$ and $q_i$ is the charge of the field $i$ under $q$.

In principle, the generation of the total asymmetry in eq. (2.2) and its transfer due to the operator (2.1) could happen simultaneously. In this case, instead of being constant, the asymmetry in eq. (2.2) is an evolving quantity which should be described by its corresponding Boltzmann Equation (BE). For definiteness and to be as model independent as possible, we do not specify the genesis mechanism at the high scale, instead, we assume that the asymmetry generation either in the DM or in the SM sector, is completed before the transfer operator (2.1) becomes effective. As we will discuss in more detail in the next section, if the reactions induced by the transfer operator get into chemical equilibrium (i.e. proceeding faster than the expansion rate of the universe) at some point, the initial conditions (e.g. where the initial asymmetry resides) become irrelevant. On the other hand, if the transfer operator never gets into chemical equilibrium, the initial conditions do play an important role.

The moment where the transfer of the asymmetry is efficient determines which conserved charge has to be studied. If this transfer happens at temperatures higher than the one of
the EW sphaleron processes freeze out ($T_{\text{EWSp}}$), the relevant conserved charge in the SM is $q = B - L$. On the other hand, if the transfer is operative at $T < T_{\text{EWSp}}$, one can directly consider $q = B$. This transfer, however, should be completed before $T \sim 1$ MeV to avoid spoiling the standard BBN predictions. Additionally, in order to make the scenario predictive, we need a further assumption: we suppose that as in the SM, there are additional fast (gauge-like) interactions among the DM sector which efficiently annihilate away the DM symmetric component ($XX \to \ldots$) and one ends up with only its asymmetric component. Without this assumption, one could still study the model but it strays away from the philosophy of this work, since the connection between the DM and the SM through the asymmetry as in eq. (1.1) is lost. Under these considerations, the value of the conserved asymmetry $Y_{\Delta q}$ is fixed by eqs. (1.1) and (2.2). For instance, for $q = B - L$ and $q = B$ one has, respectively

$$
Y_{\Delta(B-L)} = Y_{\Delta(B-L)}^0 = |(B - L)_X| Y_X^0 + Y_{(B-L)_{\text{SM}}}^0 = \left[|(B - L)_X| r \frac{m_n}{m_X} + \kappa\right] Y_{B_{\text{SM}}}^0
$$

(2.3)

and

$$
Y_{\Delta B} = Y_{\Delta B}^0 = |B_X| Y_X^0 + Y_{B_{\text{SM}}}^0 = \left[|B_X| r \frac{m_n}{m_X} + 1\right] Y_{B_{\text{SM}}}^0,
$$

(2.4)

where $\kappa$ is an order one coefficient that relates $Y_{(B-L)_{\text{SM}}}^0$ and $Y_{B_{\text{SM}}}^0$ and which depends on the relativistic degrees of freedom at $T_{\text{EWSp}}$ (e.g. $\kappa = \frac{79}{29}$ if the EW sphaleron processes freeze out before EW phase transition and assuming only the SM degrees of freedom [54]). Let us stress that, since the nucleon mass $m_n \sim 1$ GeV, the SM baryon asymmetry $Y_{B_{\text{SM}}}^0$ and the ratio of energy densities $r$ are fixed by observations; hence, for a given DM mass $m_X$, the total asymmetry (either $Y_{\Delta B}$ or $Y_{\Delta(B-L)}$) is also fixed.

In order to obtain the correct $Y_{B_{\text{SM}}}$, one has to determine the value of $\Lambda$ for each DM mass. To do so, one needs to track the transfer of the asymmetry from one sector to the other by solving numerically the BE (see appendix A):

$$
\dot{Y}_{\Delta X} = -2 \sum_{i,j,...} \left[ \gamma(XX \leftrightarrow ij \ldots) + \gamma(X \bar{i} \leftrightarrow \bar{X}j \ldots) \right] \times \left[ 2 \frac{Y_{\Delta X}}{g_X \zeta_X Y_0} - \left( \frac{Y_{\Delta i}}{g_i \zeta_i Y_0} + \frac{Y_{\Delta j}}{g_j \zeta_j Y_0} + \ldots \right) \right],
$$

(2.5)

where $\dot{Y}_i \equiv sH \gamma \frac{dY_i}{dz}$, $z \equiv m_X/T$, $H = 1.66\sqrt{g^* m_{Pl}^2 / m_X^2}$ is the Hubble expansion rate, $M_{Pl}$ is the Planck mass and $Y_0 \equiv \frac{15}{8\pi^2 g^*}$. $\gamma(ab \leftrightarrow ij \ldots)$ is the thermally averaged reaction density

\footnote{Notice that $B$ and $L$ are violated by EW sphaleron processes but the linear combination $B - L$ remains conserved. Implicitly, we assume that whatever beyond the SM mechanism which violates $B - L$ and generates a nonzero $B - L$ asymmetry is no longer operative.}

\footnote{The typical annihilation freeze out temperature is about $T \sim m_X/20$ while to avoid nucleon decay, the lowest DM mass we consider is about 2 GeV. Hence the lowest freeze out temperature in our scenario is about 0.1 GeV and this will not affect BBN which takes place at much lower temperature, around MeV. If the annihilation products are some light dark particles, due to pure redshift in their temperature after decoupling, the contribution to the dark radiation during BBN or later can be estimated from the ratio of relativistic degrees of freedom $(g_{\text{BH}}/g_{\text{decoupling}})^{1/3} \lesssim 0.1$ which is allowed by current Planck observations [2].}
for the scattering $ab \leftrightarrow ij \cdots$. For the particle $i$, $g_i$ denotes the corresponding degrees of freedom while the statistical function $\zeta_i$ is given by

$$
\zeta_i \equiv \frac{6}{\pi^2} \int_{z_i}^{\infty} dx \, x \sqrt{x^2 - z_i^2} \frac{e^x}{(e^x \pm 1)^2},
$$

(2.6)

where $z_i \equiv m_i/T$ and the $+ (-)$ sign corresponds to a fermionic (bosonic) field $i$. For relativistic particles ($z_i \ll 1$), $\zeta_i \sim 1$. Notice that from eq. (2.2), we have $\dot{Y}_{\Delta q_{\text{SM}}} = -q_X Y_{\Delta X}$, which reflects the conservation of the charge $q$. Hence, the symmetry of the system allows to describe the dynamics of the asymmetries using a single BE for either $Y_{\Delta q_{\text{SM}}}$ or $Y_{\Delta X}$: all the asymmetries on the right hand side of eq. (2.5) can be written only in terms of $Y_{\Delta q_{\text{SM}}}$ or $Y_{\Delta X}$ [55]. Once the BE (2.5) is solved and the value of $\Lambda$ (for each $m_X$) is determined, the operator (2.1) is completely fixed and one can duly calculate its phenomenological consequences which are discussed in detail in section 4. In the next section, we will consider different scenarios for the sharing of the asymmetries.

3 Scenarios for the sharing of the asymmetries

In this study, we discuss two different scenarios for the transfer processes. In the first scenario, we consider the situation where the operator (2.1) is operative and then freezes out at $T_f$, before the EW sphaleron processes freeze out at $T_{\text{EWSp}}$, i.e. $T_f > T_{\text{EWSp}}$.\footnote{There could be in-between cases where the operator eq. (2.1) can be operative at $T > T_{\text{EWSp}}$ and then freezes out at $T_f < T_{\text{EWSp}}$, but in that scenario, one loses part of the predictive power of the framework because the symmetries which relate the DM and the SM sectors are not longer the same and the relation spelled out in eq. (2.2) (or more specifically in eq. (2.3)) no longer applies. Hence we restrict the analysis to $T_f > T_{\text{EWSp}}$.} In this regime, the initial temperature $T_i$, defined to be the temperature when the total asymmetry generation is completed, depends on the unspecified UV completion of the model which the EFT cannot describe. In fact, there are solutions that strongly depend on the initial conditions (and in particular on $T_i$) and they correspond to cases where the dynamics is UV-dominated. Hence, we only consider solutions which do not depend on $T_i$, i.e. those that achieve chemical equilibrium.

In the second scenario, we consider the situation where the operator eq. (2.1) is only operative after the EW sphaleron processes freeze out. In particular, the initial temperature is taken to be $T_i = T_{\text{EWSp}}$, which we fix to $T_{\text{EWSp}} = 132$ GeV [56] and also for simplicity take this temperature to be the EW symmetry breaking scale. In this case, we have a well-defined initial temperature and can also entertain solutions in which the reactions induced by eq. (2.1) never reach the chemical equilibrium.

3.1 Before the electroweak sphaleron processes freeze out

Here we consider the scenario where the operator eq. (2.1) is relevant before the EW sphaleron processes freeze out. In this case, the relevant symmetry of the SM is $B - L$. Our minimality criteria is to consider the SM gauge invariant operators consist of only the SM fields but carry nonzero $B - L$. Then, the lowest dimensional realization of the operator $O_{\text{SM}}^{(n)}$ corresponds to $n = 5$ [57, 58].\footnote{In the following, the 2-component Weyl spinor notation is used. Notice that the operator $\epsilon_{ij} \epsilon_{kl} \left( \ell_{i\alpha} \ell_{j\beta} \right) H^k H^l = O_{\alpha\beta}^{(5)} - O_{\beta \alpha}^{(5)}$ and hence it is not independent.}

$$
O_{\alpha\beta}^{(5)} = \epsilon_{ik} \epsilon_{jl} \left( \ell_{i\alpha} \ell_{j\beta} \right) H^k H^l,
$$

(3.1)
Table 1. The coefficients relating the number asymmetries of the corresponding fields to the charge asymmetries, as in eq. (3.2).

| i | qL | uR | dR | ℓL | eR | H |
|---|----|----|----|----|----|---|
| c_i | 7/237 | -5/237 | 19/237 | -7/79 | -3/79 | -4/79 |

where ℓ_L and H are respectively the lepton and the Higgs doublets, α, β, ... label the family indices, whereas i, j, ... the SU(2)_L indices. ϵ_{ij} is the total antisymmetric tensor with ϵ_{12} = 1.

The operator \( O_{αβ}^{(5)} \) has zero \( B \) and \( L \) equals to two, which fixes \( B_X = 0 \) and \( L_X = 1 \).

3.2 After the electroweak sphaleron processes freeze out

Let us consider the scenario where the transfer is operative after the EW sphaleron processes freeze out. In this case, \( B \) and \( L \) are the effective symmetries of the system. Although \( L \) is not of interest here, an existing lepton asymmetry can affect the results as it will be shown later.
We assume that the EW symmetry is already broken and therefore that the fermions and the weak gauge bosons are massive. In this case, we have another relevant scale namely the vev of the Higgs \( v \). In our EFT approach with an effective scale \( \Lambda \), we should impose \( \Lambda \gg v \) to make sure the whole framework remains consistent. As before, our minimality criteria is to consider SM gauge invariant operators consisting of only SM fields, and carrying nonzero \( B \). The lowest dimensional realizations of the operator \( O_{SM}^{(n)} \) are those for \( n = 6 \) [57, 59–61]:

\[
\begin{align*}
O_{\alpha\beta\delta\gamma}^{(6)I} &= \epsilon_{abc} \epsilon_{ij} \left( q_{La}^{ia} \ell_{Lb}^{jb} \right) \left( d_{Rc}^{i} u_{Rd}^{j} \right), \\
O_{\alpha\beta\delta\gamma}^{(6)II} &= \epsilon_{abc} \epsilon_{ij} \left( q_{La}^{ia} q_{Lb}^{jb} \right) \left( u_{Rc}^{i} e_{Rd}^{j} \right), \\
O_{\alpha\beta\delta\gamma}^{(6)III} &= \epsilon_{abc} \epsilon_{ij} \left( q_{La}^{ia} q_{Lb}^{jb} \right) \left( u_{Rc}^{i} e_{Rd}^{j} \right), \\
O_{\alpha\beta\delta\gamma}^{(6)IV} &= \epsilon_{abc} \left( d_{Ra}^{ia} u_{Rb}^{jb} \right) \left( u_{Rc}^{i} e_{Rd}^{j} \right),
\end{align*}
\]

where \( a, b \) and \( c \) denote the color indices and \( \epsilon_{abc} \) is the total antisymmetric tensor.\(^{10}\) All the operators above have both \( B \) and \( L \) equal to one which fixes \( B_X = L_X = 1/2 \). One might also consider the dimension-7 operator \( O_{\alpha\beta\delta\gamma}^{(7)} = \epsilon_{abc} \epsilon_{ij} \left( u_{Rc}^{ia} d_{Rj}^{ba} \right) \left( \ell_{Li}^{a} d_{Rk}^{bj} \right) H^{ij} \) which upon the EW symmetry breaking gives rise to \( \epsilon_{abc} v \left( u_{Rc}^{ia} d_{Rj}^{ba} \right) \left( \ell_{Li}^{a} d_{Rk}^{bj} \right) \). For consistency, we impose \( \Lambda \gg v \) such that this operator (and other higher dimensional operators proportional to powers of \( v/\Lambda \)) is subdominant and then not considered any further.

As before, we derive the relation between the particle asymmetries and the (effective) U(1) symmetries of the system. In general, the operator (2.1) conserves total lepton number but violates individual lepton flavor numbers, and we assume that this is the case. For simplicity, we also assume that the EW symmetry is already broken and hence, one should consider the conservation of the electric charge and also take into account the effect of the masses of the SM fermions. Due to the mass terms, the chemical potential for the left- and right-handed fields become equal. Therefore, in the following, we will not differentiate the fermion chiralities: \( u = u_L = u_R \) and similarly for all the other SM fermions. The SM fields which carry nonzero chemical potentials are the up-type \( u \) and down-type \( d \) quarks, the neutrinos \( \nu \), the charged leptons \( e \) and the charged weak boson \( W \). As before, we have suppressed the family and the color indices. Hence, \( u \) refers to the \( u, c \) and \( t \) quarks; analogously, \( d \) refers to \( d, s \) and \( b \); and \( e \) refers to \( e, \mu \) and \( \tau \).

Taking the total electric charge to be zero \( (n_{\Delta Q} = 0) \) and assuming the decoupling of the top quark (\( \zeta_t = 0 \)), one can express the particle number asymmetries in terms of the charge asymmetries \( n_{\Delta B}, n_{\Delta L} \) and \( n_{\Delta X} \) as follows:

\[
\frac{n_{\Delta \zeta_i}}{g_i \zeta_i} = \frac{1}{c_0} \left( c_B^{\zeta_i} n_{\Delta B} + c_L^{\zeta_i} n_{\Delta L} + c_X^{\zeta_i} n_{\Delta X} \right),
\]

\(^{10}\)If there are right-handed neutrinos \( \nu_R^R \)'s, one could also have operator of type \( u_R d_R d_R \nu_R \). If \( \nu_R \) has no Majorana mass term (or if \( M_{\nu_R} \ll m_X \)), the sharing scenario is completely analogous to the one described by the operators (3.4)–(3.7) (up to gauge multiplicities). For \( M_{\nu_R} \gg m_X \), the sharing operator is not relevant due to Boltzmann suppression at \( T \sim m_X \). If \( M_{\nu_R} \sim m_X \), this will require a separate analysis to take into account the dependence on Majorana mass term and also the effect of washout of lepton asymmetry due to lepton-number-violating Majorana mass term. In any case, the qualitative effect could be captured by our later analysis as we consider different initial conditions for lepton asymmetry: from \( Y_{\Delta L} = -51/28 Y_{\Delta B} \) to \( Y_{\Delta L} = 0 \) to take into account various degrees of erasure of the lepton asymmetry (see section 3.3).
where \( c_0 \equiv 6 \left[ 5 + (2 + \zeta_b + \zeta_c + \zeta_s) \frac{3W}{2} + (4 + 3 \zeta_c) \zeta_b + (4 + 3 \zeta_s) \zeta_c + 4 \zeta_s \right] \), \( c_X^i = -B_X c_B^i - L_X c_L^i \), and \( c_B^i \) and \( c_L^i \) are given in table 2.

For the operators (3.4)–(3.7) we have \( B_X = L_X = 1/2 \); the BE for \( Y_{\Delta X} \) is

\[
Y_{\Delta X} = -2 \gamma_{qqq} \left[ 2 \frac{Y_{\Delta X}}{g_X \zeta_X Y_0} - \frac{1}{c_0} \frac{Y_0}{Y_0} \left( c_B Y_{\Delta B} + c_L Y_{\Delta L} - \frac{1}{2} (c_B + c_L) Y_{\Delta X} \right) \right], \tag{3.9}
\]

where

\[
c_B = 22 + 5 \zeta_s + \frac{27 \zeta_W}{2} + 5 \zeta_b + 8 \zeta_c, \tag{3.10}
\]

\[
c_L = 2 \left[ 2 + (2 + \zeta_c + \zeta_s) \frac{\zeta_W}{2} + \left( 3 + \zeta_c + \frac{\zeta_W}{2} \right) \zeta_b + (3 + \zeta_c) \zeta_s \right]. \tag{3.11}
\]

\( \gamma_{qqq} \equiv \gamma_{XX \rightarrow qqq} + \gamma_{X i \rightarrow Xqqq} + \gamma_{X \bar{q} \rightarrow Xqqq} \) denotes collectively the thermally averaged reaction densities resulted from operator (2.1) with \( O_{SM} \) given by any of the operators (3.4)–(3.7).

Although in the numerical calculations of the next section we will consider the statistical functions \( \zeta \) in eq. (2.6) for \( W, b, c \) and \( s \), it turns out that the only particle which might decouple during the evolution is \( W \) and its effect is negligible. Hence, it is a good approximation to consider the case where these particles are fully relativistic, i.e. \( \zeta_W/2 = \zeta_b = \zeta_c = \zeta_s = 1 \) with \( \{ c_0, c_B, c_L \} = \{ 228, 67, 30 \} \). Notice that \( Y_{\Delta B} \) here is fixed by observations to be \( Y_{\Delta B}^0 \) as in eq. (2.4) while the value for \( Y_{\Delta L}^0 \) is model-dependent. As before, the relevant reduced cross sections are collected in appendix B.

### 3.3 Numerical results

In principle, for each DM mass \( m_X \) one can solve the BE and find the appropriate value for \( \Lambda \) in order to distribute the asymmetries of the two sectors such that the observed DM relic abundance and the baryon asymmetry are reproduced. However, the results depend on the following assumptions:

(i) The total asymmetry. We assume that the total asymmetry is fixed by eq. (2.3) or eq. (2.4), for scenarios where the transfer of the asymmetry happens before or after the EW sphaleron processes freeze out, as described in the preceding section. In other words, the genesis of the asymmetry is already completed prior to the transfer. For the case after the freeze-out of the EW sphaleron processes, since the total lepton number

| \( i \) | \( c_B^i \) | \( c_L^i \) |
|---|---|---|
| \( u \) | \( 3 \left( 2 + \zeta_b + \zeta_s + \frac{3W}{2} \right) \) | \( 2 \left( 1 + \zeta_b + \zeta_s \right) \) |
| \( d \) | \( 3 \left( 2 + 2 \zeta_c + \frac{3W}{2} \right) \) | \( -2 \left( 1 + \zeta_c \right) \) |
| \( \nu \) | \( -2 \left( 1 - \zeta_b + 2 \zeta_c - \zeta_s \right) \) | \( 2 \left[ 3 + (2 + \zeta_b + \zeta_c + \zeta_s) \frac{\zeta_W}{2} + (2 + \zeta_c) \zeta_b + (2 + \zeta_s) \zeta_c + 2 \zeta_s \right] \) |
| \( e \) | \( 1 - \zeta_b + 2 \zeta_c - \zeta_s \) | \( 2 \left[ (2 + \zeta_b + \zeta_c + \zeta_s) \frac{\zeta_W}{2} + (1 + \zeta_c) (1 + \zeta_b + \zeta_s) \right] \) |
| \( W \) | \( 3 \left( 1 - \zeta_b + 2 \zeta_c - \zeta_s \right) \) | \( -2 \left( 2 + \zeta_b + \zeta_c + \zeta_s \right) \) |

Table 2. The coefficients relating the number asymmetries of the corresponding fields to the charge asymmetries, as in eq. (3.8).
is conserved, there is an extra dependence on the initial total lepton asymmetry. In this
case, we vary \( Y_{\Delta L} \) from \(-\frac{51}{28} Y_{\Delta B}\) to 0. The former value is set by the EW sphaleron
processes that freeze out before EW phase transition assuming the SM relativistic
degrees of freedom [54], while the latter considers the possibility of a mechanism that
erases the lepton asymmetry (after the freeze out of the EW sphaleron processes). This
variation is represented by the bands of solutions in figure 2.

\[(ii) \text{ The initial distribution of the asymmetry.} \] Even if the total asymmetry is fixed by
eq (2.3) or eq. (2.4), one has to consider whether the initial asymmetry resides in the
DM or in the SM sector. Let us remember that this discussion is only relevant in
the case where the sharing operator does not reach the chemical equilibrium. If the
chemical equilibrium is attained, the evolution of the system becomes independent of
the initial conditions. In this study, we assume that all the initial asymmetry resides
either in the DM or in the SM sector. Of course, it is also possible that part of the
initial asymmetry resides in the dark sector while the rest in the visible sector. However,
without a specific model for the asymmetry generation, this assumption appears too
contrived and also results in a loss of predictivity.

In order to explore the solutions of the BE corresponding to the cases where the asym-
metry is transferred before and after the freeze out of the EW sphalerons (sections 3.1 and 3.2,
respectively), we consider the two cases where \( X \) is a complex scalar or a Dirac fermion. For
\( X \) as a Dirac fermion, for each \( \mathcal{O}_{SM} \), there are two possible kinds of couplings, one which
involves \( X_L X_L \) and the other which involves \( X_R X_R \). For simplicity, we assume both to couple
equally. For definiteness, we further assume that DM only couples to the \textit{first family}
SM fermions in eqs. (3.1) and (3.4), and hence all the SM fermions involved can be taken
to be massless. The corresponding results for the operators (3.5)–(3.7) can be obtained by
the rescaling due to different gauge multiplicities listed in table 3 (appendix B). With the
assumption of couplings only with the first family of SM fermions, the limits from collider
searches presented in the next section are the most stringent. Furthermore, there are no flavor
violating processes. If the assumption of couplings only to the first family is relaxed, these
processes have to be taken into account. However, this introduces model dependency since
for a complete analysis, one would need to consider a UV completion for the operators (see
for instance ref. [62]). For the purpose of the present work, this possibility is not considered.

In figure 2, we show the regions, in the plane \([m_X/\Lambda, m_X]\), where the measured baryon
asymmetry of the universe and the DM relic abundance can be reproduced simultaneously, for
complex scalar (upper panel) and fermionic (lower panel) DM. In the upper left hatched parts
of the figure, the effective scale \( \Lambda \) is smaller than the Higgs vev. This region is disregarded,
as discussed in section 3.2. Moreover, during the freeze out the relevant energy scale is
\( E \sim 2 m_X \) and the perturbative constraint yields \( m_X/\Lambda \ll 2\pi \), taking the coupling to be
4\pi. In order to be conservative, in figure 2 we cut off at \( m_X/\Lambda = 1 \). For the numerical
analysis we are fixing \( r = \Omega_X/\Omega_B = 5.4 \) and \( Y_{\Delta B_{SM}} = 9 \cdot 10^{-11} \). The two scenarios discussed
previously in section 3, namely when the transfer of the asymmetry is efficient before and
after the freeze out of the EW sphalerons, are depicted in the figure.

For the scenario where the asymmetry sharing takes place before the EW sphaleron
processes freeze out, we only consider the solutions when the system achieves chemical equi-
librium during its evolution. As \( m_X \) increases, to obtain the right relic abundance, the
number asymmetry of \( X \) needs to decrease. This can be achieved by increasing the ratio
\( m_X/\Lambda \) such that the chemical decoupling happens at a later time when the number density
Figure 2. Parameter space where the measured baryon asymmetry of the universe and the DM relic abundance can be reproduced simultaneously, for complex scalar (upper panel) and fermionic (lower panel) DM, and for the scenarios where the transfer of the asymmetry is efficient before and after the freeze out of the EW sphalerons (see text). In the upper left hatched regions \( \Lambda \) is smaller than the Higgs vev.

is more Boltzmann suppressed. Notice that the increase in \( m_X/\Lambda \) is quite mild due to strong Boltzmann suppression from the increase in \( m_X \). Note that for this case to work the DM has to be heavier than \( \sim 500 \) GeV, otherwise the freeze out occurs after the EW sphaleron freeze out.

For the scenario where the transfer happens after the EW sphaleron processes freeze out, the upper and lower bounds of the bands represent the two different initial total lepton asymmetries discussed previously: \( Y_{\Delta L} = 0 \) and \( Y_{\Delta L} = -\frac{51}{28} Y_{\Delta B} \), respectively. For \( Y_{\Delta L} = -\frac{51}{28} Y_{\Delta B} \), the system never reaches chemical equilibrium, which implies a dependence on the initial conditions: the initial asymmetry can reside either in the DM or in the SM sector.
Let us first consider the scenario where all the asymmetry is stored in the dark sector. The fact that the system never reaches chemical equilibrium implies that there is no Boltzmann suppression. Hence, as $m_X$ increases, the ratio $m_X/\Lambda$ has to be strongly enhanced in order to deplete the number asymmetry of the DM (or equivalently, increase the transfer of the number asymmetry to the SM sector) to obtain the right relic abundance. In this case, the increase in $m_X/\Lambda$ has to be quite steep as $m_X$ increases. Next we consider the case where the initial asymmetry is stored in the SM sector. We found that this scenario is not viable for the following reason. In fact, the transfer from the visible to the dark sector increases the DM asymmetry, but its value cannot reach the observed one which is higher than the chemical equilibrium value.

As we raise $Y_{\Delta L} \to 0$, in the mass range $10\, \text{GeV} \lesssim m_X \lesssim 500\, \text{GeV}$ the system gets into chemical equilibrium. In this regime, the results depend quite significantly on the assumed initial lepton asymmetry. For $m_X \lesssim 10\, \text{GeV}$ or $m_X \gtrsim 500\, \text{GeV}$, the system is not able to reach chemical equilibrium and interestingly, the results become rather independent of the existing lepton asymmetry. This can be understood from the following: in this regime, the first term of the right hand side of the BE (3.9), which is independent on $Y_{\Delta L}$, becomes the dominant one; while the other terms, including the one that depends on $Y_{\Delta L}$, are subdominant. In this case where the transfer happens after the EW sphaleron processes freeze out, the DM spans a large range of masses from few GeV to $\sim 2\, \text{TeV}$.

4 Phenomenological constraints

Now we discuss several constraints and experimental opportunities due to the following two realizations of the operator (2.1):

\begin{align}
\frac{1}{\Lambda_{5-p}} XX \bar{O}^{(5)} &= \frac{1}{\Lambda_{5-p}} XX \epsilon_{ik} \epsilon_{jl} \left( \bar{\ell}_L^i \ell_L^j \right) H^k H^l, \\
\frac{1}{\Lambda_{6-p}} XX \bar{O}^{(6)I} &= \frac{1}{\Lambda_{6-p}} XX \epsilon_{abc} \epsilon_{ij} \left( \bar{d}_R^a \ell_L^j \right) \left( \bar{u}_R^c \ell_L^i \right).
\end{align}

where we have considered the coupling only to the first family SM fermion (the indices are dropped) and selected only $O^{(6)I}$ among the four operators from eqs. (3.4)–(3.7), as it has been done in the previous section. As we mentioned before, the results for the operators (3.5)–(3.7) can be obtained through the rescaling due to the different gauge multiplicities as specified in table 3 (appendix B); though the phenomenological signatures can be different (for instance, in some cases they involve only charged leptons while in others only neutrinos).

Furthermore, let us note that the requirement of fast $XX$ annihilations in general gives rise to both DM direct detection and collider signatures which, however, are model-dependent. On the other hand, this kind of processes do not contribute to the DM indirect detection because there is only either X or $\bar{X}$ today (i.e. DM is maximally asymmetric). Since the present shared asymmetry scenario cannot restrict this type of operators, we will not consider them further besides assuming that they are efficient enough to remove the DM symmetric component.

4.1 Collider

The operator (4.1) can lead to measurable signatures at colliders. At the LHC, one can have the vector boson scattering with production of two same-sign leptons together with two jets and missing transverse energy: $pp \to W^\pm W^{\pm} jj$ and from our operator we will have
Figure 3. Inclusive cross sections for monojet and missing transverse energy with (light pink) and without (blue) monolepton for scalar (first row) and fermionic (second row) DM at the LHC, for a center of mass energy of 8 TeV (first column) and 13 TeV (second column). The blue solid line corresponds to the ATLAS exclusion limit on monojet searches; the dashed lines to the conservative limits for the break down of the EFT description (see text).

$W^+ W^+ \rightarrow e^+ e^+ XX$ and the conjugate process. There are dedicated searches at ATLAS [63, 64] and CMS [65, 66] that can be used in order to constraint this scenario. The study of this process will be included in an upcoming work [67]. Furthermore, one could also have $e^- e^- \rightarrow W^- W^- XX$ and the conjugate process, however, this requires an electron-electron or a positron-positron lepton collider, which will not be available in the near future.

On the other hand, the operator (4.2) gives rise to two types of signatures at the LHC:

(a) monojet with missing energy;

(b) monojet plus monolepton and missing energy.

There are several features due to that operator that we would like to highlight. First, for processes involving a charged lepton in the final state, we can further distinguish between $pp \rightarrow j e^+ + E_T^{miss}$ and $pp \rightarrow j e^- + E_T^{miss}$. In particular, the production cross section of the latter at the LHC is about two to three orders magnitude more suppressed than the former, purely due to scarcity of antiquarks in the proton. This type of asymmetry is a distinguished feature of our scenario. Hence, we will only focus on the dominant process $pp \rightarrow j e^+ + E_T^{miss}$. Secondly, due to the steep energy dependence of the cross section of our operator $\sigma \propto E_T^{(5-p)} / \Lambda^{2(6-p)}$, the LHC will be more sensitive than direct and indirect searches. For fermionic DM ($p = 1$),
the production cross section at the LHC is further enhanced. This can be understood as follows: equating the cross sections for fermion and scalar DM during the asymmetry transfer \( (E \sim m_X) \), we have \( \Lambda_{10}^{\text{fermion}} \sim E^2 \Lambda_8^{\text{scalar}} \sim m_X^2 \Lambda_8^{\text{scalar}} \). Hence taking the ratio of fermion to scalar DM cross section at the LHC, we have \( E^8 / \Lambda_{10}^{\text{fermion}} \times \Lambda_8^{\text{scalar}} / E^6 = E^2 / m_X^2 \) enhancement (see figure 3). Thirdly, the two types of signatures \((a)\) and \((b)\) depend on the same coupling and hence one can utilize a more sensitive channel to constraint our scenario.

In figure 3, we show the total production cross sections for \((a)\) (blue bands) and \((b)\) (light pink bands) at the LHC with a center of mass energy \( \sqrt{s} = 8 \text{ TeV} \) (left panels) and 13 TeV (right panels), using the solutions presented in figure 2. We also plot the line of \( \Lambda = \sqrt{s}/(4\pi) \) to show the estimations below which the effective operator description could break down for the LHC at \( \sqrt{s} = 8 \text{ TeV} \) (dashed-dotted lines) and 13 TeV (dashed lines). The effective description breaks down at lower energy if the coupling is smaller. We have assumed the most conservative value for the typically transferred energy to be the maximum value i.e. \( \sqrt{s} \). Here we do not consider the unitarity bound which we expect to be of a similar order [68].

Based on monojet searches by ATLAS [69] and CMS [70], we provide an estimate on the upper bound on cross section. Using \text{MadGraph5}_\text{aMC@NLO} [71], we estimate the efficiency times acceptance \( \epsilon \times A \) and the most sensitive regime by imposing a cut on the final quark transverse momentum, which in this case, is equivalent to \( E_T^{\text{miss}} \). From the ATLAS and the CMS analysis, we determine the most sensitive regimes to be \( E_T^{\text{miss}} > 600 \text{ GeV} \) and \( E_T^{\text{miss}} > 550 \text{ GeV} \) which give an upper bound on \( \epsilon \times A \) to be 3.8 fb and 7 fb at 95\% CL, respectively. Our estimation gives \( \epsilon \times A \sim 0.5 \) which implies the upper bounds \( \sigma \sim 3.8 \text{ fb}/0.5 = 7.6 \text{ fb} \) and \( 7 \text{ fb}/0.5 = 14 \text{ fb} \). In figure 3, the solid blue line refers to the ATLAS exclusion limit on monojet searches, which is more stringent. This bound will weaken once we do the full analysis since the efficiency will be lower [67]. In the lower left panel of figure 3 is shown that the monojet searches at LHC with 8 TeV (horizontal solid blue line) can already constrain a part of the parameter space of fermionic DM, corresponding to masses between \( \sim 12 \text{ GeV} \) and \( \sim 70 \text{ GeV} \). However, that region is very close to the zone where we conservatively estimate our EFT approach to break down (indicated by the dashed-dotted lines) and a UV description would be required. In this regime, the EFT is not reliable because the LHC could in principle resolve our effective operators to reveal new heavy degrees of freedom. However, one could still use EFT description by applying the truncation method i.e. by removing high momentum transfer events which violate the EFT to derive a weaker bound [72–76]. Alternatively, one could use UV complete models for analysis to obtain model dependent bounds (e.g. on new heavy states). A more comprehensive analysis including constraints from monolepton searches (e.g. ref. [77]) with a UV complete model will be presented in ref. [67]. Finally, in figure 4, we translate the EFT bounds and ATLAS limit of 7.6 fb on monojet searches at 8 TeV to the \( [m_X / \Lambda, m_X] \) plane.

4.2 Dark matter indirect detection

For DM indirect detection, both operators (4.1) and (4.2) can give rise to observable astrophysical signatures. From the operator (4.1), the possible annihilation channels are: \( XX \rightarrow \nu \nu \), \( XX \rightarrow \nu h \), \( XX \rightarrow \nu \nu h h \) and \( XX \rightarrow e^- e^- W^+ W^+ \) and the conjugate process, where \( \nu \) and \( h \) are respectively the SM neutrino and the Higgs boson.\(^{11}\) The first process dominates over the others which have additional phase space suppression. Hence,\(^{11}\)

\(^{11}\) In our sharing scenario, the sign of the \( B - L \) asymmetry in the DM sector is the same as the one of the SM sector (which is positive). Hence we will be left with only \( \bar{X} \) today and their annihilations will necessarily contain antineutrinos in the final states [41].
let us consider the thermal averaged cross section $\langle \sigma v \rangle_{XX \rightarrow \nu\nu}$. Even for the most optimistic point in our parameter space $m_X = 400$ (500) GeV (indicated by the stars in figure 4), we have $\langle \sigma v \rangle_{XX \rightarrow \nu\nu} \sim 5 \times 10^{-32}$ cm$^3$/s for $X$ being a complex scalar (Dirac fermion). This value is about nine orders of magnitude smaller than the current sensitivities of the IceCube [78, 79] and the ANTARES [80] experiments.

Similarly for the operator (4.2), the annihilation $XX \rightarrow 3$ quarks + 1 lepton gives rise to potentially observable fluxes of gamma rays, neutrinos, positrons, etc. For the most optimistic case of $m_X \sim 2$ TeV, we determine $\langle \sigma v \rangle_{XX \rightarrow 3\text{ quarks} + 1\text{ lepton}} \sim$ few $10^{-30}$ cm$^3$/s for both complex scalar and fermionic DM. This is about four orders of magnitude far from the current sensitivities of detectors like VERITAS [82], H.E.S.S. [83] or MAGIC and Fermi-LAT [84], which are closing in around the thermal cross section for standard WIMP DM $\langle \sigma v \rangle_{\text{WIMP}} \sim$ few $10^{-26}$ cm$^3$/s [85]. Hence, currently or in the near future, the possibilities of probing this scenario via indirect detection are very challenging. We want to stress that this conclusion does not hold when the effective operator description does not apply (e.g. in the proposal in ref. [53]), where one can indeed have promising indirect signatures.

### 4.3 Dark matter direct detection

The operator (4.1) generates inelastic scatterings of the type $X + \text{nucleon} \rightarrow \bar{X} + \text{nucleon} + 2 \nu$ through a Higgs exchange. Since neutrinos can carry away momenta, the kinematic for this process is different from the usual 2-to-2 scattering and the sensitivity of the experiment should decrease. One can do an estimation on the spin independent cross section $\sigma_{X-n}$ by comparing the scalar $X$ scenario to theScalar Singlet DM model (SSDM) [86, 87] (also happening via a Higgs exchange), as follows

$$\frac{\sigma_{X-n}}{\sigma_{\text{SSDM}}} \sim \frac{1}{\lambda_{\text{HP}}^2} \left( \frac{m_X}{\Lambda} \right)^6 \frac{2^3 \pi}{211 \pi^5},$$  (4.3)

\text{In fact, ref. [81] pointed out that for $m_X$ greater than $\sim 200$ GeV, one could obtain up to an order of magnitude stronger bounds utilizing the gamma-ray flux generated from EW bremsstrahlung.}
where \( \lambda_{HP} \sim \mathcal{O}(10^{-2}) \) is the Higgs-portal coupling in the SSDM. Considering the most optimistic points for \( m_X = 400 \text{ GeV} \) and \( m_X / \Lambda = 0.07 \), one obtains \( \sigma_{X-n}^{ssm} \sim 10^{-8} \) (for the fermionic \( X \), the ratio will be similarly suppressed). This is much smaller than any experimental sensitivities and put us well within the regime where the coherent neutrino scattering background becomes relevant \[88\].

For the operator (4.2), although we have restricted the analysis to \( 2m_X > m_n \) such that the nucleon decay is kinematically forbidden, one might have to consider the possibility of an induced nucleon decay (IND) as originally proposed in ref. \[52\]. However, due to baryon number conservation, there is no IND in the shared asymmetry scenario as we explain in the following. First let us define the SM baryon asymmetry to be positive. Then for the system which achieves chemical equilibrium as shown on the left panel of figure 1, the net baryon asymmetry has to be positive which also implies that the DM asymmetry has to be positive. From the operator (4.2), \( B_X = 1/2 \) and hence we are left with only \( X \) today. Also the same operator causes the IND: \( \bar{X} + p \rightarrow X + e^+ \), \( \bar{X} + n \rightarrow X + \bar{\nu}_e \), \( \bar{X} + p \rightarrow X + \pi^0 \) and \( \bar{X} + n \rightarrow X + \pi^0 \); and since there is no \( \bar{X} \) present today, these processes cannot happen.\[13\] On the other hand, in the case where the DM and the SM sectors never get into chemical equilibrium, the initial distribution of the asymmetries become relevant. Since we assume that the initial total asymmetry is stored in either one of the sectors (e.g. on the right panel of figure 1), its sign has to be the same as the SM baryon asymmetry, which is positive. Therefore, we are left with only \( X \) today and as before, IND cannot occur. In the case where non-equilibrium dynamics generates asymmetries equal in magnitude and opposite in sign in the visible and DM sectors, the DM with opposite sign baryon number today can result in IND \[52, 89-92\]. In these scenarios, unlike in the shared asymmetry case, the transfer operators need to always be out of equilibrium, otherwise the asymmetry would be washed out.

5 Conclusions

In this work, we have considered the case where DM is a singlet under the SM gauge interactions but carries nonzero baryon and/or lepton numbers. In this case, the DM can be asymmetric just like the SM baryons, and the asymmetries could be shared. We assumed then the DM to be maximally asymmetric, and either a complex scalar or a Dirac fermion. The DM mass spans the range between few GeV and \( \sim 100 \text{ TeV} \). The connection between the dark and the visible sectors was described by effective operators in the context of an EFT, and it was separated in two different regimes depending on whether the transfer of the asymmetries was effective before or after the EW sphaleron processes freeze out. The main difference between these two regimes is the following: before the EW sphaleron processes freeze out the relevant symmetry is \( B - L \), while after the EW sphaleron processes freeze out \( B \) and \( L \) become separately the appropriate symmetries. The leading operators consisting of only the SM fields come in a limited number: one dim-5 operator with \( B - L \) charge and four dim-6 operators with \( B \) charge. This feature makes the present scenario predictive in the following sense. For a given DM mass, the total conserved asymmetry is fixed by the measurements of the ratio of energy densities \( \Omega_X / \Omega_B \) and the SM baryon asymmetry \( Y_{B_{SM}}^0 \); the main role of the effective operators is to distribute the asymmetry between the visible and the dark sectors. Furthermore, the requirement of obtaining the correct sharing (the observed DM

\[13\] One can ponder about processes like \( X + \text{nucleon} \rightarrow X + 2 \text{nucleons} + \text{lepton} \), but this cannot occur due to kinematics.
relic abundance and the SM baryon asymmetry) fixes the Wilson coefficients of the operators. Once the coefficients are fixed, one can determine the phenomenology of this scenario.

Regarding possible signatures at different facilities, we found that while DM indirect and direct detection are very challenging to current experimental searches, the LHC is already probing relevant parts of the parameter space. This fact is due to the steep energy dependence of our operators. The LHC phenomenology for this model is very rich and goes out of the scope of the present work. We will dedicate a detailed analysis in an upcoming work [67].

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A Derivation of the Boltzmann equations

First we review the approximations made in relating the number density asymmetry of a particle $i$ to its chemical potential. The number density for $i$ can be obtained by integrating its phase space distribution $f_i$ over the 3-momentum as follows [93]

$$n_i = g_i \int \frac{d^3p}{(2\pi)^3} f_i,$$

(A.1)

where $g_i$ denotes the relevant degrees of freedom (e.g. spin and gauge). In general, $f_i$ is a generic function that needs to be solved from the BE. Nevertheless, if the particle $i$ is involved in fast elastic scatterings (through for instance gauge interactions), the kinetic equilibrium is established and $f_i$ takes the equilibrium phase space distribution (that of Bose-Einstein or Fermi-Dirac) given by

$$f_{eq}^i = \frac{1}{e^{(E - \mu_i)/T} - \eta_i},$$

(A.2)

with $\eta_i = 1(-1)$ for $i$ boson (fermion). If the particle $i$ is also involved in fast inelastic scatterings with the corresponding gauge bosons $G$ as $i + \bar{i} \rightarrow G$, where $\bar{i}$ denotes the antiparticle of $i$, one has $\mu_i + \mu_{\bar{i}} = 0 \Rightarrow \mu_{\bar{i}} = -\mu_i$, since the gauge bosons have zero chemical potential.\(^{14}\) In this case, the number density asymmetry of $i$ can be determined in terms of its chemical potential as follows

$$n_{\Delta i} \equiv n_i - n_{\bar{i}} = g_i \int \frac{d^3p}{(2\pi)^3} \left( f_{eq}^i - f_{eq}^{\bar{i}} \right)$$

$$= \frac{g_i}{2\pi^2} \int_{m_i}^{\infty} dE E \sqrt{E^2 - m_i^2} \left[ \frac{1}{e^{(E - \mu_i)/T} - \eta_i} - \frac{1}{e^{(E + \mu_i)/T} - \eta_i} \right].$$

(A.3)

For the early universe, the number density asymmetry for a particle is much smaller than its equilibrium number density and hence $\mu_i/T \ll 1$ always holds. However in the non-relativistic regime, since the equilibrium number density is Boltzmann suppressed, $\mu_i/T \ll 1$.

\(^{14}\)This is the case for all the SM particles and also for the DM particle $X$ which is assumed from the outset to participate in fast interactions which annihilate away the symmetric component.
might no longer hold. One can numerically check from eq. (A.3) that even if the chemical freeze-out happens as late as \(T \sim m_i/25\), for \(m_i \gtrsim 1\) GeV and imposing the correct DM asymmetry, one can still guarantee that \(\mu_i/T \lesssim 0.05\). In our asymmetry sharing scenario, such a late freeze-out only occur for extremely heavy \(m_i\) and hence \(\mu_i/T \ll 0.05\). So one can expand eq. (A.3) in term of \(\mu_i/T \ll 1\) and keep only the leading term\(^{15}\)

\[
n_{\Delta i} = \frac{T^3}{6} g_i \zeta_i \frac{\mu_i}{T},
\]

where we have defined
\[
\zeta_i = \frac{6}{\pi^2} \int_{z_i}^{\infty} dx \, x \sqrt{x^2 - z_i^2} \frac{e^x}{(e^x - \eta_i)^2},
\]

with \(z_i \equiv m_i/T\). In the relativistic limit \(z_i \ll 1\), we have \(\zeta_i \sim 1\) (2) for \(i\) being a fermion (boson) while in the nonrelativistic limit \(z_i \gg 1\), we obtain \(\zeta_i = \frac{6}{\pi^2} z_i^2 \mathcal{K}_2(z_i)\) for both fermions and bosons, where \(\mathcal{K}_2\) is the modified Bessel function of the second kind of order 2. For later convenience, we further define the abundance as
\[
Y_a = \frac{n_a}{s},
\]

where \(s = \frac{2\pi^2}{45} g_* T^3\) is the entropic density and \(g_*\) the effective entropic degrees of freedom (\(g_* = 106.75\) when all the SM particles are relativistic). Finally, we can rewrite eq. (A.4) as

\[
\frac{\mu_i}{T} = \frac{1}{2} \frac{n_{\Delta i}}{g_i \zeta_i n_0} = \frac{1}{2} \frac{Y_{\Delta i}}{g_i \zeta_i Y_0},
\]

where we have defined \(n_0 \equiv \frac{T^3}{12}\) and \(Y_0 \equiv \frac{n_0}{s} = \frac{15}{8\pi^2} g_*\).

Now we proceed to derive the BE used in this work. In the radiation-dominated early universe described by the Friedmann-Lemaître-Robertson-Walker metric, the evolution of the number density of particle \(a\) for a general process \(a + b + \ldots \leftrightarrow i + j + \ldots\) is described by \(^{[93]}\)

\[
\dot{Y}_a = - \sum_{b, \ldots; i, j, \ldots} [ab\ldots \leftrightarrow ij\ldots],
\]

where we have defined \(\dot{Y}_a \equiv s H z \frac{dY_a}{dz}\) with \(z \equiv m/T\), \(m\) some arbitrary mass scale and the Hubble expansion rate given by
\[
H = \sqrt{\frac{4\pi^3 g_*}{45} \frac{T^2}{M_{Pl}^2}},
\]

where \(M_{Pl} = 1.22 \times 10^{19}\) GeV. The right-handed side of eq. (A.8) is the collision term given by

\[
[ab\ldots \leftrightarrow ij\ldots] \equiv \Lambda^{ij\ldots}_{ab\ldots} \left[\mathcal{M}(ab\ldots \rightarrow ij\ldots) f_a f_b \ldots (1 + \eta_i f_i) (1 + \eta_j f_j) \ldots \right. \nonumber \\
- \left. \mathcal{M}(ij\ldots \rightarrow ab\ldots) f_i f_j \ldots (1 + \eta_a f_a) (1 + \eta_b f_b) \ldots \right].
\]

\(^{15}\)Notice that in the expansion, there are only terms with odd power in \(\mu_i/T\) as expected, since a change of sign in the chemical potential corresponds to a change of sign in the asymmetry number density, as shown in eq. (A.3). Interestingly, for massless particles, the series truncates at \((\mu_i/T)^3\).
where
\[ \Lambda_{ab...}^{ij...} \equiv c_{PSI}c_{PSF} \int d\Pi_a d\Pi_b \ldots d\Pi_i d\Pi_j \ldots (2\pi)^4 \delta^{(4)} (p_a + p_b + \ldots - p_i - p_j - \ldots) , \]  
\[ d\Pi_a \equiv \frac{d^3 p_a}{(2\pi)^3 2E_a} . \]  
(A.11)

In the above, \(|M(ab\ldots \rightarrow ij\ldots)|^2\) is the squared amplitude \textit{summed} over initial and final degrees of freedom (the additional factor in Wick’s contraction for identical particles in the operator is implicitly taken into account). For later convenience, we explicitly write down \(c_{PSI}\) and \(c_{PSF}\) to denote the respective compensating factors when there are identical particles in the initial and final states in order to avoid over-counting their contributions to the phase space. For instance, for \(n\) identical particles in the initial or final states, we have a factor of \(c_{PSI} = 1/n!\) or \(c_{PSF} = 1/n!\), respectively.

For a process \(ab\ldots \leftrightarrow ij\ldots\), using eq. (A.2) and energy conservation \(E_a + E_b + \ldots = E_i + E_j + \ldots\), the phase space distributions with vanishing chemical potentials \(f^\text{eq,0}_i \equiv f^\text{eq}_i (\mu_i = 0)\) obey the identity
\[ F^\text{eq,0} = f^\text{eq,0}_a f^\text{eq,0}_b \ldots (1 + \eta_i f^\text{eq,0}_i) (1 + \eta_j f^\text{eq,0}_j) \ldots \]  
\(= f^\text{eq,0}_i f^\text{eq,0}_j \ldots (1 + \eta_i f^\text{eq,0}_a) (1 + \eta_j f^\text{eq,0}_b) \ldots , \]  
(A.13)

Eq. (A.10) can be further rewrite as
\[ [ab\ldots \leftrightarrow ij\ldots] = \gamma (ab\ldots \rightarrow ij\ldots) \frac{f_a f_b \ldots (1 + \eta_i f_i) (1 + \eta_j f_j) \ldots}{F^\text{eq,0}} - \gamma (ij\ldots \rightarrow ab\ldots) \frac{f_i f_j \ldots (1 + \eta_i f_a) (1 + \eta_j f_b) \ldots}{F^\text{eq,0}} , \]  
(A.14)

where we have defined the thermal averaged reaction density as
\[ \gamma (ab\ldots \rightarrow ij\ldots) \equiv \Lambda_{ab...}^{ij...} |M(ab\ldots \rightarrow ij\ldots)|^2 F^\text{eq,0} . \]  
(A.15)

For the moment, the quantity above is just schematic since in eq. (A.14) all the \(f_i\) implicitly contain the momenta to be integrated over. Hence, we need the following approximations:

1. Ignore the corrections from Fermi-blocking and Bose-enhancement factors by setting
\[ \frac{1 + \eta_i f_i}{1 + \eta_i f^\text{eq,0}_i} \rightarrow 1 . \]  
(A.16)

2. If particles \(i, j, \ldots\) are in kinetic equilibrium (i.e. if \(f_{i,j,\ldots}\) take the form of eq. (A.2)) and the conditions \(\mu_{i,j,\ldots}/T \ll 1\) apply, one can expand up to linear term in their chemical potentials as follows
\[ \frac{f_i f_j \ldots}{f^\text{eq,0}_i f^\text{eq,0}_j \ldots} = 1 + \frac{\mu_i}{T} + \frac{\mu_j}{T} + \ldots = 1 + \frac{1}{2} \frac{Y_{\Delta i}}{g_i \zeta_i Y_0} + \frac{1}{2} \frac{Y_{\Delta j}}{g_j \zeta_j Y_0} + \ldots , \]  
(A.17)

where in the second equality eq. (A.7) has been used.
With the above approximations, all the energy-momentum dependent terms which multiply eq. (A.15) in eq. (A.14) drops out, and eq. (A.15) becomes a well-defined quantity. Now we are ready to derive the quantities we are interested in, which are the two types of scattering processes: $[XX \leftrightarrow ij \ldots]$ and $[\bar{X}i \leftrightarrow \bar{X}j \ldots]$, where $X$ is massive while the rest of the particles are massless. Applying the approximations (A.16) and (A.17), and keeping up to first order in number asymmetry densities, one has

$$
[XX \leftrightarrow ij \ldots] = \gamma (XX \rightarrow ij \ldots) \left( \frac{Y_{\Delta X}}{g_X \zeta_X Y_0} - \frac{1}{2} \frac{Y_{\Delta i}}{g_i \zeta_i Y_0} - \frac{1}{2} \frac{Y_{\Delta j}}{g_j \zeta_j Y_0} - \ldots \right), \quad (A.18)
$$

$$
[X\bar{i} \leftrightarrow \bar{X}j \ldots] = \gamma (\bar{X}i \leftrightarrow X\bar{j} \ldots) \left( \frac{Y_{\Delta X}}{g_X \zeta_X Y_0} - \frac{1}{2} \frac{Y_{\Delta i}}{g_i \zeta_i Y_0} - \frac{1}{2} \frac{Y_{\Delta j}}{g_j \zeta_j Y_0} - \ldots \right). \quad (A.19)
$$

For the CP conjugate processes $[\bar{X}X \leftrightarrow \bar{i}j \ldots]$ and $[\bar{X}i \leftrightarrow X\bar{j} \ldots]$, one simply has to flip the signs of all number density asymmetries (i.e. chemical potentials). Since in this context the CP violation is not relevant, one can consider the tree level processes where $\gamma (XX \rightarrow ij \ldots) = \gamma (\bar{X}X \rightarrow \bar{i}j \ldots)$ and $\gamma (\bar{X}i \leftrightarrow X\bar{j} \ldots) = \gamma (\bar{X}i \leftrightarrow X\bar{j} \ldots)$. The BE for $Y_X$ and $Y_{\bar{X}}$ are simply

$$
\dot{Y}_X = -2 \sum_{i,j,...} [XX \leftrightarrow ij \ldots] - \sum_{i,j,...} \left( [X\bar{i} \leftrightarrow X\bar{j} \ldots] - [\bar{X}i \leftrightarrow X\bar{j} \ldots] \right), \quad (A.20)
$$

$$
\dot{Y}_{\bar{X}} = -2 \sum_{i,j,...} [\bar{X}X \leftrightarrow \bar{i}j \ldots] + \sum_{i,j,...} \left( [X\bar{i} \leftrightarrow \bar{X}j \ldots] - [\bar{X}i \leftrightarrow X\bar{j} \ldots] \right). \quad (A.21)
$$

Finally, the BE for $Y_{\Sigma X} \equiv Y_X + Y_{\bar{X}}$ and $Y_{\Delta X} \equiv Y_X - Y_{\bar{X}}$ can be written down as follows

$$
\dot{Y}_{\Sigma X} = -2 \sum_{i,j,...} \left( [XX \leftrightarrow ij \ldots] + [\bar{X}X \leftrightarrow \bar{i}j \ldots] \right) = 0, \quad (A.22)
$$

$$
\dot{Y}_{\Delta X} = -2 \sum_{i,j,...} \left( [XX \leftrightarrow ij \ldots] - [\bar{X}X \leftrightarrow \bar{i}j \ldots] \right)
-2 \sum_{i,j,...} \left( [X\bar{i} \leftrightarrow X\bar{j} \ldots] - [\bar{X}i \leftrightarrow X\bar{j} \ldots] \right)
= -2 \sum_{i,j,...} \left[ \gamma (XX \rightarrow ij \ldots) + \gamma (\bar{X}i \leftrightarrow X\bar{j} \ldots) \right]
\times \left[ \frac{2}{g_X \zeta_X Y_0} \left( \frac{Y_{\Delta i}}{g_i \zeta_i Y_0} + \frac{Y_{\Delta j}}{g_j \zeta_j Y_0} + \ldots \right) \right]. \quad (A.23)
$$

Notice that $Y_{\Sigma X}$ is constant up to $\mathcal{O}(Y_{\Delta X})$. Since we have assumed $X$ to participate in fast scattering e.g. $XX \rightarrow \ldots$, $Y_{\Sigma X} = 2Y_X^{eq}$ up to $\mathcal{O}(Y_{\Delta X})$ throughout the evolution. So at the leading order in $Y_{\Delta X}$, one only needs to solve the BE for $Y_{\Delta X}$.

## B Reduced cross sections

For a 2-to-$N$ body scattering, from eq. (A.15) one has that the reaction density

$$
\gamma (ab \rightarrow ij \ldots) \equiv \Lambda_{ab}^{ij\ldots} |\mathcal{M}(ab \rightarrow ij \ldots)|^2 f_a^{eq} f_b^{eq} \left( 1 + \eta_i f_i^{eq} \right) \left( 1 + \eta_j f_j^{eq} \right) \ldots. \quad (B.1)
$$
Ignoring the Fermi-blocking and the Bose-enhancement factors, and taking all the phase space distribution to be Maxwell-Boltzmann, one has\footnote{These approximations allow to express eq. (B.1) as the integral of a standard scattering cross section. Notice that however, the squared amplitude is summed over both the initial and the final degrees of freedom (no averaged over the initial degrees of freedom). Otherwise, one just has to evaluate eq. (B.1) directly.}

\[
\gamma (ab \rightarrow ij \ldots) = c_{PS} \int d\Pi_a d\Pi_b 2s \beta \left(1, \frac{m_a^2}{s}, \frac{m_b^2}{s}\right) \sigma_{ab\rightarrow ij \ldots}(s) e^{-(E_a + E_b)/T}, \tag{B.2}
\]

where the cross section is

\[
\sigma_{ab\rightarrow ij \ldots}(s) = c_{PS} \frac{1}{2s\beta \left(1, \frac{m_a^2}{s}, \frac{m_b^2}{s}\right)} \int |\mathcal{M}(ab \rightarrow ij \ldots)|^2 d\Phi_N, \tag{B.3}
\]

with \(d\Phi_N \equiv (2\pi)^4 \delta^{(4)}(P_a + P_b - P_i - P_j - \ldots) d\Pi_i d\Pi_j \ldots\) being the \(N\)-body phase space element and

\[
\beta(1, v, w) \equiv \sqrt{(1 - v - w)^2 - 4vw}. \tag{B.4}
\]

With some algebra one can rewrite eq. (B.2) in a more convenient form in term of only the center of mass energy \(\sqrt{s}\) and the temperature \(T\) of the thermal bath as follows

\[
\gamma (ab \rightarrow ij \ldots) = c_{PS} \frac{T}{64\pi^4} \int_{s_{\text{min}}}^{\infty} ds \sqrt{s} \tilde{\sigma}_{ab\rightarrow ij \ldots}(s) K_1 \left(\frac{\sqrt{s}}{T}\right), \tag{B.5}
\]

where \(s_{\text{min}} = \max \left((m_a + m_b)^2 (m_i + m_j + \ldots)^2\right)\), \(K_1\) is the modified Bessel function of the second kind of order 1 and the dimensionless reduced cross section is

\[
\tilde{\sigma}_{ab\rightarrow ij \ldots}(s) \equiv 2s \left[\beta \left(1, \frac{m_a^2}{s}, \frac{m_b^2}{s}\right)\right]^2 \sigma_{ab\rightarrow ij \ldots}(s). \tag{B.6}
\]

Finally eq. (B.5) can be rewritten in a more convenient form in term of \(z = m/T\) with \(m\) a convenient mass scale as follows

\[
\gamma (ab \rightarrow ij \ldots) = c_{PS} \frac{m^4}{64\pi^4 z} \int_{x_{\text{min}}}^{\infty} dx \sqrt{x} \tilde{\sigma}_{ab\rightarrow ij \ldots}(x) K_1 \left(\sqrt{x} z\right), \tag{B.7}
\]

with \(x \equiv s/m^2\) with \(x_{\text{min}} = s_{\text{min}}/m^2\).

### B.1 Dark matter as a complex scalar \(\phi\)

In the following the mass of complex scalar \(\phi\) is taken to be \(m_\phi\) while \(f\) and \(b\) denote respectively a massless Weyl fermion and a complex scalar. First, the relevant reduced cross sections (eq. (B.6)) that arise from an operator of the type \(\phi f b f b\) are

\[
\tilde{\sigma}_{\phi f f b b}(x) = c_G c_S c_{PS} \frac{m_\phi^6}{\Lambda^6} \beta \left(1, x^{-1}, x^{-1}\right) \frac{1}{211 \pi^5} \frac{x^3}{72}, \tag{B.8}
\]

\[
\tilde{\sigma}_{\phi b b f f}(x) = c_G c_S c_{PS} \frac{m_\phi^6}{\Lambda^6} \beta \left(1, x^{-1}, 0\right) \frac{1}{211 \pi^5} F_{\phi b b f f}(x), \tag{B.9}
\]

\[
\tilde{\sigma}_{\phi f f b b}(x) = c_G c_S c_{PS} \frac{m_\phi^6}{\Lambda^6} \beta \left(1, x^{-1}, 0\right) \frac{1}{211 \pi^5} F_{\phi f f b b}(x), \tag{B.10}
\]
Table 3. Multiplicity factors assuming that the operators only involve the first family SM fermions (the family indices in the operators are dropped). For \( c_{PS_F} \) and \( c_{PS_I} \), the first entry is for scattering of the type \( XX \rightarrow ijk\ell \) while the second entry is for \( Xi \rightarrow \bar{X} jk\ell \). Here \( X \) is either a complex scalar \( \phi \) or a Dirac fermion \( \psi \).

Where \( x \equiv s/m_\phi^2 \) and

\[
F_{\phi_{\phi_{\phi_{\phi}f_{f}f_{f}f_{f}}}f_{f_{f}f_{f_{f}}}}(x) = \frac{1}{144x^2} (x - 1)^2 \left(4x^4 + 159x^3 + 239x^2 + 19x - 1\right)
\]

\[
-\frac{1}{24} (x - 1) (x^2 + 4x + 2) \ln x.
\]  

In the above, besides the compensating factor from final state phase space \( c_{PS_F} \), we have explicitly displayed the possible gauge degrees of freedom \( c_G \) and symmetry factor \( c_S \) from Wick’s contraction when there are identical particles in the operator. The multiplicity factors for the operators (3.1), (3.4)–(3.7) are listed in table 3.

From the operator of the type \( \phi_{\phi_{\phi_{\phi}f_{f}f_{f}f_{f}}}f_{f_{f}f_{f_{f}}}, \) the relevant reduced cross sections are

\[
\hat{\sigma}_{\phi_{\phi_{\phi_{\phi}f_{f}f_{f}f_{f}}}f_{f_{f}f_{f_{f}}}}(x) = c_G c_S c_{PS_F} \frac{m_\phi^8}{\Lambda^8} \beta(1, x^{-1}, x^{-1}) \frac{1}{2440x^2} x^4 
\]

\[
\hat{\sigma}_{\phi_{\phi_{\phi_{\phi}f_{f}f_{f}f_{f}}}f_{f_{f}f_{f_{f}}}}(x) = c_G c_S c_{PS_F} m_\phi^8 \Lambda^8 \beta(1, x^{-1}, 0) \frac{1}{2440x^2} F_{\phi_{\phi_{\phi_{\phi}f_{f}f_{f}f_{f}}}f_{f_{f}f_{f_{f}}}}(x),
\]

where

\[
F_{\phi_{\phi_{\phi_{\phi}f_{f}f_{f}f_{f}}}f_{f_{f}f_{f_{f}}}}(x) = \frac{(x - 1)^2 (4x^4 + 159x^3 + 239x^2 + 19x - 1)}{1440x^2}
\]

\[
-\frac{1}{24} (x - 1) (x^2 + 4x + 2) \ln x.
\]  

B.2 Dark matter as a Dirac fermion \( \psi \)

Here \( \psi \) denotes a Dirac fermion with mass \( m_\psi \) while \( f \) and \( b \) denote respectively a massless Weyl fermion and a complex scalar. From the operator of the type \( \psi_{\psi_{\psi_{\psi}f_{f}f_{f}b_{b}}b_{b_{b}}}, \) the relevant
reduced cross sections are

\[ \hat{\sigma}_{\psi\psi ffbb}(x) = c_G c_S c_{PS} \frac{m_\psi^8}{\Lambda^8} \beta \left(1, x^{-1}, x^{-1}\right) \frac{1}{2^{11} \pi^5} \frac{(x-4)x^3}{36} , \]

(B.16)

\[ \hat{\sigma}_{\psi\psi\psi ffb}(x) = c_G c_S c_{PS} \frac{m_\psi^8}{\Lambda^8} \beta \left(1, x^{-1}, 0\right) \frac{1}{2^{11} \pi^5} F_{\psi\psi\psi fb}(x) , \]

(B.17)

\[ \hat{\sigma}_{\psi\psi\psi fb}(x) = c_G c_S c_{PS} \frac{m_\psi^8}{\Lambda^8} \beta \left(1, x^{-1}, 0\right) \frac{1}{2^{11} \pi^5} F_{\psi\psi\psi fb}(x) , \]

(B.18)

where \( x \equiv s/m_\psi^2 \) and

\[ F_{\psi\psi\psi fb}(x) \equiv \frac{1}{4320x^3} (x-1)^2 (5x^6 - 135x^5 - 3012x^4 - 4062x^3 - 387x^2 + 33x - 2) + \frac{7}{72} (3x^2 + 10x + 5) \ln x. \]

(B.19)

From the operator of the type \( \psi\psi ffff \), the relevant reduced cross sections are

\[ \hat{\sigma}_{\psi\psi ffff}(x) = c_G c_S c_{PS} \frac{m_\psi^{10}}{\Lambda^{10}} \beta \left(1, x^{-1}, x^{-1}\right) \frac{1}{2^{11} \pi^5} \frac{(x-4)x^4}{360} , \]

(B.21)

\[ \hat{\sigma}_{\psi\psi ffff}(x) = c_G c_S c_{PS} \frac{m_\psi^{10}}{\Lambda^{10}} \beta \left(1, x^{-1}, 0\right) \frac{1}{2^{11} \pi^5} F_{\psi\psi\psi fff}(x) , \]

(B.22)

where

\[ F_{\psi\psi\psi fff}(x) \equiv \frac{1}{4320x^3} (x-1)^2 (5x^6 - 135x^5 - 3012x^4 - 4062x^3 - 387x^2 + 33x - 2) + \frac{7}{72} (3x^2 + 10x + 5) \ln x. \]

(B.23)

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