Downhole distributed acoustic sensing reveals the wavefield structure of the coastal microseisms

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Abstract

Ocean-generated seismic waves are omnipresent in passive seismic records around the world and present both a challenge for earthquakes observations and an input signal for interferometric methods for characterisation of the Earth’s interior. Understanding of these waves requires the knowledge of the depth-dependence of the oceanic noise at the transition into continent. To this end, we examine 80 days of continuous acquisition with Distributed Acoustic Sensor (DAS) system deployed in two deep boreholes near the south-eastern coast of Australia. The data has excellent Signal-to-Noise Ratio (SNR) in a range from 0.03Hz to over 100Hz. By analysing the seismograms and correlation with wave climate, the DAS response are confidently decomposed into the microseisms generated by swell from remote storms (~0.15Hz) and local winds (between 0.3Hz and 2Hz), and strong body waves energy from large surf break at the coast (from 2Hz to 20Hz). The depth dependence of the microseisms allows for robust normal modes analysis of the Rayleigh waves with only one borehole. The results of this analysis agree with the data from conventional dense seismological arrays. Overall, we found that the link between the amplitudes at each channel

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along the borehole and wave climate is so strong and stable that with sufficient amount of training data, the passive seismic records on downhole DAS may be used for high-precision monitoring of both formations surrounding the borehole and remote storms in the ocean.

**Keywords:** oceanic microseisms, distributed acoustic sensing, passive seismic monitoring

1. **Introduction**

Motion of water in stormy seas induces omnipresent ambient seismic wavefield in the frequency band from $\sim 0.01\text{Hz}$ to $\sim 20\text{Hz}$ (Webb 1998). These frequencies overlap with the frequency band of earthquake signals critical for seismological observations by Ocean Bottom Stations (OBS), and hence has often been regarded as unwanted noise (e.g., Webb 1998). Over the years, a link has been established between some components of the ocean-generated microseisms and wave climate in stormy seas (McCreery et al., 1993; Bromirski et al., 1999; Bromirski and Duennebier, 2002; Aucan et al., 2006), which allows the seismic observations to be used for monitoring the sea conditions and the rock properties in the vicinity of the sensor. Furthermore, rapid development of interferometric methods expanded the research focus to the subsurface characterisation using passive seismic data (e.g., Nakata et al., 2019). However, inversion of the passive seismic observations often assumes stationary isotropic wavefield (Wapenaar et al., 2010). This assumption is invalid for ocean-generated seismic energy, which is highly directional and depends on the current sea conditions (Bromirski and Duennebier, 2002; Gerstoft et al., 2006). A more accurate knowledge of the mechanisms responsible for generation of the seismic signals can significantly improve the accuracy of the estimated subsurface properties (e.g., Delaney et al., 2017).

Global OBS networks provide the main means to study the seismic wavefield generated by the ocean (Webb 1998; Stephen et al., 2003). These data sets feature two clear signals: primary, or Single Frequency (SF), microseisms at a
peak frequency of the ocean waves and a much stronger Double Frequency (DF) microseisms at twice that frequency. The SF energy is related to the transfer of water surface oscillations into elastic energy through a direct interaction of the water waves with ocean floor (Hasselmann 1963), and hence the intensity of these signals drops exponentially with the water depth. Typically SF microseisms become undetectable a few kilometers into the continent Haubrich and McCamy 1969; Bromirski and Duennebier 2002. In turn, DF microseisms originate from nonlinear interaction of ocean wave trains of a similar frequency and opposite direction (Longuet-Higgins and Jeffreys 1950; Hasselmann 1963; Kibblewhite and Wu 1991). The resulting oscillations penetrate almost lossless to the sea bottom and couple into leaky Rayleigh wave modes, which dominate the low-frequency part of the seismic noise on land. Amplitudes of the seismic waves depend on the storm parameters in a large source region and the seismic properties of the ocean bottom (Webb 1992; Tanimoto 2007; Ardhuin et al. 2013; Gimbert and Tsai 2015).

Overall, the mechanisms generating the seismic waves at the ocean bottom are relatively well understood, although a quantitative prediction of the microseisms remains a challenging problem. At the same time, transition of the microseisms into the continent is poorly understood. Conventional seismological arrays are too sparse for the ambient seismic wavefield (~10km). As a result, we only have coarse scale distribution of the velocities and intensity of the propagating coherent signals from the kinematic and polarization analysis (Gerstoft et al. 2006; Brooks et al. 2009; Nakata et al. 2019). Moreover, depth-dependency of the seismic amplitudes is rarely available (Dorman and Prentiss 1960), because seismic sensors are deployed either on the ground or in very shallow boreholes (<100m) when the anthropogenic or other noise at the deployment site is high. Sometimes, ocean-related ambient noise is recorded in few points in a subsurface by microseismic arrays designed for fluid-induced seismicity in geological formations (e.g., Vaezi and van der Baan 2014) or mines stability (Dolgikh et al. 2020). Without sufficient areal coverage and snapshots of the subsurface amplitude distribution, dynamics of rapidly changing ambi-
ent seismic wavefield at the coast remains uncertain. Numerical simulations of this process are computationally expensive and are based on poorly constrained models of the subsurface and seismic source, and are able to capture only well-established features of the microseisms such as dependence on water depth or presence of the soft sediments at the bottom (Levchenko et al., 2011; Ying et al., 2014).

Distributed acoustic sensor (DAS) arrays based on fiber-optic technology offer a new way of multi-channel seismic acquisition in a broad frequency range capable of continuous recording of seismic wavefields and their spatial distribution. Recently, Lindsey et al. (2017); Yu et al. (2019) reported successful field tests of DAS measurements for seismological applications. DAS records have excellent Signal-to-Noise Ratio (SNR) for teleseismic earthquakes that have similar frequency content to the ocean noise. Lindsey et al. (2020); Williams et al. (2019) used communication optical fibre cables on shallow ocean bottom to characterize the microseism field. These measurements are however confined to the water-sediments transition boundary and hence provide only limited information about the propagation of the microseisms field deeper into the subsurface. More detailed information may be obtained from measurement of a DAS system in a sufficiently deep borehole. With the rapid development of the borehole seismic monitoring using DAS (e.g., Correa et al., 2017; Egorov et al., 2017), the instrumented wells may be employed for ambient seismic monitoring.

This paper analyses ambient seismic wavefield in 80 days of continuous DAS acquisition by two boreholes with a depth of over 1500 m near the south-eastern coast of Australia. First, we describe the available data set and establish a link between traditional point sensors for displacement (seismometers and geophones) and DAS measurements. Second, we identify the physical nature of the seismic signals on DAS and their relationship with the wave climate using spectral characteristics and travel-time curves along the borehole. Then, analysis of the depth-dependence of the microseisms amplitudes along the borehole provides an estimate of the energy partition between the normal modes of the Rayleigh wave. In the end, we outline some unique capabilities and limitations
of the DAS measurements in deep boreholes for monitoring both subsurface properties and wave climate.

2. The data set

Ambient seismic wavefield was recorded from 21 October 2018 to 07 December 2019 by DAS systems in CRC-2 and CRC-3 wells (see fig. 1b). These wells have been drilled as a part of the CO2CRC Otway Project, Australian pilot research project focused on the geological sequestration of CO2 \cite{Cook2014}. The Otway Project site is located at the shore of the Southern Ocean in the Australian State of Victoria, approximately 240km west of Melbourne (fig. 1a).

Several closely spaced wells ∼1600m deep have been drilled and instrumented with modern DAS systems. Seismic properties in the vicinity of the wells are available from sonic logs and numerous 3D borehole and surface seismic surveys with active sources \cite{Glubokovskikh2016, Egorov2017, Egorov2018}.

Our analysis of the oceanic noise relies on remarkable performance of the modern DAS systems in a broad frequency range, especially at low frequencies \cite{Lindsey2017}. The seismic measurements by DAS estimate a rate of the axial deformation of the optical fibre $\epsilon_{zz}$ induced by a seismic wave. To this end, a DAS interrogator measures the phase difference between laser pulses backscattered from adjacent segments of the optical fibre. Appendix \ref{appendix:A} presents an original derivation of the measurement principle implemented in iDASv3™ and iDASv2™ systems manufactured by Silixa (Elstree, Hertfordshire, UK, \url{http://www.silixa.com}), which are deployed in CRC-3 and CRC-2 wells, respectively. CRC-2 has a previous generation DAS system, which uses a standard single-mode optical communication fibre deployed on the production tubing. As a result, CRC-2 DAS records feature much higher instrumentation noise than the data from CRC-3, which has the cable cemented behind the casing (fig. 2). Note that the increased noise in the uppermost ∼270 m of both wells is due to surface casing, which causes intense mechanical reverberations of seismic signals.
Figure 1: Outline of the experiment: elevation map (a) showing the positions of the monitoring well (blue circle) instrumented with distributed acoustic sensing system, CRC-3 well, and WAVESWATCHIII wave buoys (red triangles) of Victoria (Australia), and satellite image of the CO2CRC Otway Project site (b) with the position of the seismic recording system.
In the following, we focus on the CRC-3 records. The seismic signal on DAS deployed in CRC-3 may be converted into the particle displacement along the fibre $u_z$ using factor $F_{\text{DAS}}(k_z)$ derived in appendix A. The factor depends on the frequency $\omega$ of seismic signals and parameters of instrumentation: distance along the fibre between the reflection points of the backscattered pulse known as gauge length $L_0$, duration of the pulse $\tau$, and speed of light $c$ in the fibre material. For small $k_z$, a projection of the seismic wave vector on the fibre, equation (A.10) for the DAS response reduces to

$$F_{\text{DAS}}(k_z) = -\frac{L_0\tau c}{4} (\omega \cdot k_z).$$

(1)

Equation (1) shows that for most types of seismic waves, the DAS sensitivity drops with decreasing frequency relatively quickly, as $\omega^2$. However, the phase interferometry approach implemented in iDASv3™ provides sufficient SNR starting from a few millihertz. Pevzner et al. (2020a) showed that eq. (1) holds true for the DAS system in CRC-3 and the data still provides clear records of teleseismic earthquakes. In the following sections we divide the spectral amplitude of the DAS response by $\omega$, to make DAS data more consistent with the conventional seismological records, which measure either particle displacement or its temporal derivatives, velocity and acceleration.

3. DAS response versus wave climate

The DAS record in CRC-3 (fig. 2a) shows an abundance of ambient seismic energy at all depth levels. The Otway site is located in the area of active farming; previous analysis (Pevzner et al., 2020b) showed DAS records containing distinct anthropogenic noise: monochromatic signals from various farming machinery, impulse sources, and even routine movement of cattle. Yet, the records are dominated by low-frequency surface waves with an apparent period $\sim$2s propagating horizontally and frequently repeated body waves and their scattered modes with an average period below 0.5s propagating at an angle to the borehole receiver array. In the following we show that these signals are generated by the ocean.
Figure 2: A fragment of raw seismic data records in the CRC-3 well (a) and CRC-2 well (b). The record starts at 05:17:15 UTC on the 15th of November 2018. Vertical scale corresponds to the measured depth along the boreholes, as both wells are nearly vertical. The stronger noise in the top 270m in both wells is due to the surface casing.

Figure 3 compares the low-frequency seismic response in CRC-3 with the oceanic wave climate (WAVEWATCH III monitoring system [https://polar.ncep.noaa.gov/waves/hindcasts/nopp-phase2.php](https://polar.ncep.noaa.gov/waves/hindcasts/nopp-phase2.php)). Since records on all of the nearby buoys are very similar, in the following we only show data from WBAST1 buoy. Qualitatively, we see that storms – distinguished by high wind speed $W_S$ and significant wave height $H_S$ – correspond to high intensity of the DAS response in the range from 0.1 to 2Hz. The peak magnitude persistently occurs at $\sim 0.6$Hz. According to the frequency dependence of the correlation coefficients (fig. 4a), we divide the DAS records into several groups:

1. $< 50$mHz: no ocean-related energy detectable;
2. from 50mHz to 120mHz: gradual increase of the ocean-related microseisms;
3. $\sim 150$mHz: classical DF microseisms;
4. $\sim 0.3$Hz to 2Hz: local microseisms;
5. from 2Hz to 20Hz: frequently recurring body waves;
6. $> 20$Hz: vibrations of the recording unit caused by local wind.

In group I microseisms, if any, are weaker than the instrumental noise.
Figure 3: Comparison of the low frequency response on distributed acoustic sensing data in CRC-3 against the wave climate recorded by buoy WBAST1 (see fig. 1a): the ocean wave spectrogram (Welch 1967 average for 3a -hour segment with 30 min window) (bottom panel); spectrogram of the seismic response divided by angular frequency $\omega$ (Welch 1967 average for a 2-hour segment with 5 min window an 50% overlap), where the white lines correspond to the 10db and 15db contours of the ocean wave spectrum plotted in doubled frequency scale (middle panel); significant wave height and wind speed and direction (top panel). The red arrows indicate arrivals of strong teleseismic earthquakes.
Figure 4: Relationship between the strength of the seismic response at a depth of 300m in the CRC-3 well and wave climate at the coast: correlation coefficient of the wind speed and significant wave height with the power spectrum density (dB scale) of seismic signals computed with the 0.01Hz spacing (a); temporal variation of the wind speed, significant wave height and intensity of the classical double frequency microseisms, local microseisms and body waves excited by surf break normalized to their standard deviation.
Between 50mHz and 120mHz, although the correlation coefficients gradually increase, the intensity of the primary microseisms at ∼70mHz is relatively low and a peak at <0.1Hz only seldom appears in the data. Group 6 contains high-frequency clutter, which is unlikely to come from the ocean. Indeed, seismic Q in the area is about 100 or smaller (Pirogova et al., 2019), and hence these waves would attenuate substantially at distances on the order of several kilometers. Instead, signals at frequencies over 20Hz may be caused by wind-induced mechanical vibrations of the hut housing the recording unit. We omit a further discussion of groups 1, 2 and 6 because they are affected by characteristics of the acquisition system, rather than the ambient seismic field. In the remaining frequency range, 0.1Hz - 20Hz, the DAS data stably provides high SNR as evident from high correlation with features of the wave climate.

The correlation peak for $H_S$ at ∼150mHz corresponds to twice the peak ocean wave frequency and hence represents the classical DF microseisms. These seismic signals are studied extensively in the literature and our data agree with numerous reports from around the world (e.g., Webb, 2007; Bromirski and Duennebier, 2002 [Nakata et al., 2019]): the contours of the buoy spectrum plotted versus double frequency capture the structure of the DAS spectrum up to 0.2 Hz (see fig. 3). Interestingly, correlation with $W_S$ drops noticeably at this frequency, which merely indicates significant contribution of the swell arriving from remote storms into the local wave climate. These microseims arrive at CRC-3 well as a plane surface wave with relatively high magnitude at all depths and polarity reversal at ∼700m (see fig. 5a).

Unlike the DF microseims, strong energy in group 4 is uncommon for the passive seismic records. For the range between ∼0.3Hz and 2Hz, the correlation is high for both $H_S$ and $W_S$, which suggests that the microseisms are generated by local wind waves. A similar correlation of the microseisms with local wind has been reported for ocean bottom stations in the east Pacific ocean, and seismometers in Iceland (Bromirski et al. 1999) and Hawaii (McCreery et al. 1993, Garcés et al., 2006). Ocean waves depend on the strength, duration and size of the storm (Pierson Jr. and Moskowitz, 1964). Strong low frequency
(~15s period) waves require stably strong winds over an extended area, while formation of high frequency ocean waves occurs relatively quickly: around 5 hours for 4s period. During the data acquisition, minimum wind speed was 4m/s and the average speed 8m/s, which should be sufficient to 'saturate' the part of the wave spectrum corresponding to periods from 1s to 6s [Pierson Jr. and Moskowitz 1964]. The local microseisms travel as a surface wave with depth dependence of amplitudes very similar to the DF microseisms (fig. 5b).

Group 5 has frequencies that cannot be directly related to the frequency of ocean waves. Yet they show strong correlation of the seismic amplitudes to the amplitudes of ocean waves, but not with the wind speed. [Garcés et al. 2006; Aucan et al. 2006; McCrery et al. 1993] reported similar observations on coastal stations and some evidence that the seismic energy in the range between 2Hz and 20Hz is caused by abrupt impacts of breaking surf at the coast. Our data agree with this hypothesis. The filtered seismograms contain clearly visible recurring body wave arrivals (fig. 5c), with travel-time curves indicating waves propagating at an angle to the surface. Indeed, reverberations of shear waves are ubiquitous in the soft carbonate sediments in the upper 60m. Furthermore, pairs of compressional and shear waves arrive from beneath CRC-3 with almost constant time delay. A detection algorithm based on matching the compressional and shear travel-time curves has identified about 60,000 such events over 70 days of recording. The behaviour of correlation coefficients in this frequency band indicates that the abundance and strength of these events is controlled by the significant wave height.

A peculiar feature of the DAS records in CRC-3 is a steadily high strength of the microseisms at 0.6Hz, while traditionally seismic records are dominated by signals with frequency equal to twice the peak frequency of ocean waves [Webb 1998; Nakata et al. 2019]. Commonly accepted models (e.g., Pierson Jr. and Moskowitz 1964) predict that with increasing wind speed, the short-period ocean waves reach maximum intensity quickly, while progressively lower-frequency waves become stronger with increasing wind speed. Therefore, the wave height energy and hence microseisms spectrum decrease rapidly with
increasing frequency. It is believed that above 0.3 Hz, microseisms have a worldwide constant Holu spectrum (McCreery et al., 1993; Bromirski et al., 1999). But the nonlinear generation of the microseisms requires interaction of ocean waves of a similar frequency and opposite direction. Hence the strength of DF microseisms at each frequency, expressed as the power spectral density of the vertical displacement $I(\omega)$, depends on the distribution of the intensity of ocean waves $A(\omega/2, \theta)$ over azimuth $\theta$. With a few reasonable assumptions, the relationship has the following simple form (see equation (7) in Webb, 1992)

$$I(\omega) \propto \omega \cdot \int_0^\pi A(\omega/2, \theta)A(\omega/2, \theta + \pi)d\theta.$$  

(2)

The buoy data in the area shows the tendency of the high-frequency ocean waves to form pairs of sufficiently strong opposing wavetrains (see fig. 6). Predicted frequency spectra of the microseisms are in good agreement with the theoretical predictions of eq. (2). This suggests that the peak frequency in the DAS response may be a consequence of the peculiar wave climate at the Victorian coast. The frequency shift may be further increased due to factor $k_2$ in the DAS response (see eq. (1)), which increases with frequency.

4. Variation of strain with depth in the microseisms

Spectrogram in fig. 7a shows a typical intensity distribution of the DAS measurements along the CRC-3 borehole: first, amplitudes decrease towards a pronounced minimum at $\sim$700m depth; then the amplitudes increase steadily towards the bottom of the well. The minimum corresponds to the polarity reversal as seen in fig. 5a and fig. 5b for CRC-3 and in the raw data for CRC-2 well (fig. 2). Since CRC-2 and CRC-3 have different well designs and different DAS recording systems, the common features of the seismic record indicate that the seismograms bear only small overprint of the acquisition system and accurately represent the wavefield structure of the microseisms.

A commonly accepted hypothesis is that ocean-induced microseisms travel predominantly as Rayleigh waves, with the energy partition between the normal
Figure 5: A typical example of the ocean-generated noise in the seismic records in the CRC-3 well. The raw seismogram from fig. 2a is filtered (Ormsby filter) in three frequency bands: 0.1Hz - 0.2Hz (a) corresponds to the double frequency response to the peak in the ocean wave spectrum; 0.3Hz - 2Hz (b) corresponds to local microseisms; 2Hz - 20Hz (c) corresponds to the energy induced by surf breaks, where arrows indicate the travel-time curves for different components of the wavefield. The stronger noise in the top 270m in both wells is due to the surface casing.
Figure 6: Comparison of the observed microseisms with theoretical prediction in CRC-3 at 300m true vertical depth. The top row shows typical examples of directional ocean wave spectra. At the bottom, power spectral density in the DAS data is plotted against the theoretically predicted $I(\omega)$ using eq. (2), which is normalized to the measured DAS response at 0.6Hz to facilitate the comparison. The directional spectra correspond to WBAST1 buoy (see fig. 1a).
Figure 7: Variation of the intensity of the seismic response in distributed acoustic sensing measurements in CRC-3 well. Spectrogram (a) is computed using [Welch, 1967] approach within 4 hours and 10 minute window, the segment starts at 04:00:00 on the 15th of November 2018. Normal modes for frequency of 0.6Hz (b) are computed using the velocity model for the CRC-3 well (c). The rest of the panel (c) compares the observed vertical distribution of the power spectral density of the seismic measurements and a best-fit linear combination of the normal modes (the coefficients are normalised to the magnitude of the first mode). Note that the spectra are compensated for the effect of frequency. The noise in the top 270m in both wells is due to the surface casing.
modes controlled by the parameters of the source region: frequency of the ocean waves and bathymetry (e.g., Ewing et al. 1957). However, transition of the excited normal modes into the continent is a much more complicated process, which depends on onshore geology. Thus, an accurate estimate of the magnitude of the microseisms would require the knowledge of the location of the source region and the wave climate in that region along with the bathymetry and elastic properties of the sediments and crustal rocks (Hasselmann, 1963; Webb, 1992; Tanimoto, 2007; Gimbert and Tsai, 2015; Ardhuin et al., 2013). Such a comprehensive modelling is impractical with the available data and lies beyond the scope of this paper. However it is still possible to find a best-fit combination of the normal modes that may be supported by the Otway subsurface properties distribution.

To this end, we assume a 1D layered subsurface structure, where the upper 1600m have the seismic properties available from CRC-3 well logs and vertical seismic profiles (Pirogova et al., 2019) while deeper parts are based on regional seismic transects (Collins, 1988). To find the normal modes (see example in fig. 7b), we numerically integrate the differential equations that govern vertical dependence of the stress and displacements constrained by the stress-free boundary conditions and radiation principle (Aki and Richards, 2002). Figure 7c shows the measured depth curves and best-fit theoretical curves corresponding to the frequency peaks in fig. 7a. In general, the estimated amplitudes of the first three modes agree with existing analytical models (Webb, 1992; Ardhuin et al., 2013; Gimbert and Tsai, 2015). At frequencies below 0.2Hz, the fundamental mode is the most energetic component of the microseisms wavefield. Then, as the frequency increases, the higher modes become more important with the fundamental mode vanishing entirely at 0.6Hz. These results agree qualitatively with the estimates obtained for dense passive seismic arrays elsewhere (Haubrich and McCamy, 1969; Gerstoft et al., 2006; Ardhuin et al., 2013). However, those studies reported significantly lower intensity of the microseisms at frequency >0.3Hz, while in our data, the peak occurs at ~0.6Hz.

Another feature of the measured DAS intensity is a clear dependence on the
stiffness of surrounding rocks. In fig. 7b we may clearly identify the peaks and troughs corresponding to stiff and soft geological formations. Similar behaviour was observed in the analysis of amplitudes along CRC-3 of compressional waves from remote earthquakes (Pevzner et al., 2020a). Unlike the stress traction, vertical strain is discontinuous at the lithological boundaries, and hence its fine-scale variability reflects the variation of the stiffness of rocks along the borehole.

5. Discussion

We see the main merit of the present study in showing a great potential of the downhole DAS records for the analysis of ambient seismic wavefield. Thanks to the improved backscattering characteristics of the engineered optical fibres and high sensitivity and robustness of the laser pulse interferometry implemented in iDASv3™ system, these records have excellent SNR in the frequency range from 100mHz to over 100Hz, which covers almost all types of ocean-generated seismic signals. The physical nature of the observed signals could be clearly determined from their kinematic, amplitude and spectral parameters in the seismograms. Compared with traditional means for passive seismic monitoring, we see two limitations of our data set. First, we were unable to obtain confident characteristics of very low frequency signals <40mHz, including infragravity oscillations known as Earth’s hum (e.g., Webb, 2007). Nevertheless, we believe that the acquisition settings may be adjusted to provide a stronger response in millehertz range, because our data set contains clear signal from numerous teleseismic earthquakes and primary microseisms at these frequencies. Moreover, a similar DAS has been successfully used to monitor very slow strain due to changes of hydraulic head in boreholes (Becker et al., 2017). Second, DAS provides only axial strain, and thus precludes a polarization analysis of the recorded signals. Moreover, DAS has strong directivity pattern - its sensitivity deteriorates rapidly with the angle between the optical fibre and direction of wave propagation (Bona et al., 2017). At the same time, DAS may be seen as a valuable addition to arrays of existing seismological monitoring systems, as it provides the only means for
imaging of the subsurface wavefield.

Besides the parameters of the ocean surface, transition of the microseisms energy into the continent depends on the bathymetry, elastic properties of the rocks at and beneath the bottom, their attenuation and geological section onshore. We think that the latter two factors may play an important role in our observations. The wavefield in the upper 600m of the record is clearly different from the lower part: a decreased stiffness of the sediments along with a strong reflector at 600m may serve as a waveguide for the low frequency signals. A set of numerical simulations may help evaluate the importance of the local geological structure. But again, the simulation would require a realistic source function, because modelling with simple impulsive sources may provide only coarse structure of the wavefield (Levchenko et al., 2011; Ying et al., 2014), which lacks sufficient detail for our purposes. Another unknown for accurate modelling of the microseisms is seismic attenuation in the sediments at sub-Hz frequencies, which can alter the frequency content of the microseisms as they propagate inland.

The first step towards an adequate source function is the location of the source region, which is impossible with a single well. The Otway Project site has five wells instrumented with iDASv3™ systems (Pevzner et al., 2020c), within a distance of 2km. Even such a small aperture may be sufficient to accurately delineate the source regions, and hence, establish a link between the ocean parameters and seismic signal, similar to Bromirski et al. (1999); Bromirski and Duennebier (2002). For a multi-well DAS array, we will have a separate link for each channel (depth) and each well. Also, since the fine-scale variation of the strain measurements by DAS is directly related to the stiffness of the surrounding rocks, passive seismic records may become a means for repeat elastic logging of the formation changes. With ever-growing recognition of the value of downhole DAS systems, this technology may become an important subsurface surveillance tool.
6. Conclusions

This study demonstrated a substantial potential of passive seismic records obtained with a downhole distributed acoustic sensing system for studying the ocean-generated seismic signals. The data acquired at the CO2CRC Otway Project site has high signal-to-noise ratio for frequencies from 10mHz to 100Hz. Below 20Hz, the intensity of the seismic response has a clear correlation with the wave climate in the nearby ocean. Frequencies above 20 Hz correspond to vibrations of the recording system induced by local wind. Below 100mHz, we have detected numerous teleseismic earthquakes, but were unable to extract a consistent ocean-generated seismic energy.

With only one vertical borehole, analysis of the seismic amplitude distribution with depth was sufficient for confident identification of the physical nature of the signals in each frequency band. Between 2Hz and 20Hz, large surf breaks induce body waves with amplitudes and frequency of occurrence directly proportional to the significant height of the ocean waves. On the other hand, low frequency microseisms have two components: the classical double frequency component at a twice the frequency of the dominant ocean waves (∼0.15Hz) and local microseisms that correlate with local winds (∼0.6Hz). This observation is at variance with a commonly-accepted hypothesis of a worldwide constant Holu spectrum. However, this discrepancy is fully explained by the analysis of local winds, which induce high frequency wave trains moving in opposite directions, whose nonlinear interaction becomes an efficient generator of microseisms.

The microseisms have a very specific amplitude variation with depth at all frequencies and for variety of the source regions in the ocean: the surface waves change polarity at the same depth where rock stiffness changes dramatically. Such stability suggests a strong dependence of microseisms structure on the geological section in the immediate vicinity of the borehole. Normal modes analysis shows that observed amplitude variation with depth requires relatively strong contribution from higher Rayleigh modes even at low frequencies (∼100mHz).

A more comprehensive analysis of the ocean-generated seismic signals re-
quires a better control of the source contribution into the response on distributed acoustic sensing data. However, the link between the amplitudes at each channel along the borehole and wave climate appears so strong and stable that with sufficient amount of training data, the passive seismic records may be used for high-precision monitoring of both formations surrounding the borehole and remote storms in the ocean.

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Appendix A. DAS measurements of the seismic signals

This section aims to introduce the Distributed Acoustic Sensing (DAS) measurements to a broader audience. A rigorous derivation of the DAS response to the fibre vibration involves a relatively sophisticated apparatus of statistical optics (e.g., Goodman [2015]). However, essential elements of the DAS technology may be explained by a simple 1D convolutional model for the intensity of laser pulses backscattered from the fibre, which underlies the interpretation of
Optical Time Domain Reflectometry (OTDR). We analyse the optical field $E(t')$ emerging at the beginning of the fibre due to the backscattering of a pulse $s(t')$, where $t'$ is a two-way travel-time. This travel-time is related to the distance to a reflection point $z = ct'/2$, where $c$ is a speed of light in the fibre (typically, 1m corresponds to 10ns). With some reasonable assumptions, the backscattered field may be modelled as a linear function of the fibre reflectivity $r(z)$

$$E(t') = s(t') * r(ct'/2), \quad (A.1)$$

where $*$ denotes the convolution operator. We assume an idealised laser source that generates a monochromatic pulse of temporal frequency $\omega$ and width $\tau$.

Note, eq. (A.1) is true for a clean fibre, where transmitted pulses undergo negligible distortion of the phase and amplitude, and multiple scattering effects are negligible.

In the presence of time-dependent displacements $u(z, t)$, the reflectivity becomes a function of $v(z, t) = \frac{\partial u}{\partial t}$, a relative particle displacement velocity at different parts of optical fiber at a moment in time $t$. To retrieve $v(z, t)$ induced by a seismic wave, DAS systems must accurately measure the temporal variation of the OTDR intensity $I(t') = E^2(t')$. The main challenge for a practical implementation of the OTDR-like approach is generation of stable laser pulses, otherwise temporal fluctuations of $s(t)$ would obscure any signal due to $v(z, t)$.

In communication networks, OTDR uses incoherent pulses, and its output is insensitive to variations of the optical phase along fiber. But even with the best existing laser sources, the coherent OTDR can provide only qualitative estimates of the particle velocity $v(\cdot)$.

In all the quantitative DAS approaches, the effect of fibre movement on the reflected optical field is estimated using interferometric techniques (Hartog, 2017). The main idea is to compare pulses reflected at adjacent points on the fibre. Interference of these pulses is controlled by the reflection coefficients and their relative movement, but a specific form of the DAS response depends on the instrumentation configuration. Figure A.8 illustrates an implementation of this approach using an interferometer with a delay line of length $2L_0$. In the
interferometer, the pulses are duplicated into the straight and delay lines, and
the delayed pulse interferes with a pulse that was reflected from a point offset by \(L_0\) and then passed through the straight line. Thus, \(L_0\) is often called a
gauge length, a key parameter that controls the spatial resolution of the DAS
measurements.

First, we derive an optical response to a uniform displacement velocity
\(v(z, t) = v_0 \delta(z - z_0)\) at a single point \(z_0\) along the fibre (\(\delta(\cdot)\) denotes a Dirac delta
function). This approach represents the well-known dualism, when a change in
interference can be considered either as a result of a phase change or as a fre-
quency beats due to a Doppler shift (\?). The pulse \(s_2\) reflected from \(z_0\) has
a time-dependent phase shift, which may be interpreted as a Doppler shift in
frequency \(\Omega = \pm v_0 \omega / c\), where the positive sign corresponds to contraction of
the fibre and negative to the extension. First, \(s_2\) interferes with a pulse \(s_1\) com-
ing out of the delay line, then, \(s_2\) that passed through the delay line interferes
with \(s_3\) coming out of the straight line. For the first interference, the intensity
observed in a photodetector, \(I_{12}\), may be expressed as

\[
I_{12}(t') = (r_1^2 + r_2^2 + 2r_1 r_2 \cos(\Omega t')) \cdot s_2^2(t' - 2z_0/c),
\]  
(A.2)

A similar expression describes the second interference \(I_{23}\). Equation \(\text{(A.2)}\)
shows that the absolute value \(|v_0|\) defines the beat frequency of the photon
counts. For example, the magnitude of the oscillations \(I_{12}\) of \(\frac{\partial I_{12}(t)}{\partial t}\) may be
expressed as

\[
I_{12}(z) \propto s_2^2(z - z_0) \rho^2(z_0) \cdot v_0,
\]  
(A.3)

where the time dependence is converted into a distance along the fibre using a
new parameter \(\rho(z) \sim \sqrt{r(z)r(z - L_0)}\), which approximates \(r(z)\) if the reflect-
vivity varies slowly.

The proposed simple implementation of the DAS measurement in fig. \(\text{A.8}\)
is useful for understanding the principle, but it may provide only the absolute
value of the displacement velocity along the fibre. The retrieval of the sign
of \(v\) requires a more complicated system; conceptually it replaces the simple
differentiator after the photodetector in fig. A.8 with a so called ‘strain analyser’, which performs a more involved transformation of the interfering signals.

The effect of a distributed displacement velocity field \( v(z) \) on the DAS response, \( A(z) \) may be represented as a superposition of the point reflections with a Doppler shift towards each other \( \Delta \Omega(z) = \omega/c \cdot [v(z) - v(z - L_0)] \). Hence, we may think of \( I_\Omega \) as a point spread function of the DAS measurements, although the measurements involve a few nonlinear transformations. So the resultant equation for the DAS response is

\[
A(z) = I_\Omega(z) * v(z) = s_0^2(z) * \rho^2(z) * [v(z) - v(z - L_0)].
\]

(A.4)

For slow variation of the displacement velocity field along the fibre \( \gg L_0 \), eq. (A.4) shows that DAS response is proportional to an axial strain rate of the fibre \( \dot{\varepsilon}_{zz} = \frac{\partial v(z,t)}{\partial z} \).

Equation (A.4) shows that the effect of the fibre deformation bears an overprint of the spatial variations of the reflectivity along the fibre. The approach to removal of the effect of \( r(z) \) constitutes the main difference between iDASv3™ and iDASv2™ systems. The reflectivity in a conventional single-mode fibre is associated with Rayleigh scattering on low-contrast fluctuations of the optical refraction index, an inherently random process. Strictly speaking, elimination of this random effect would require an ensemble of the DAS measurements for the same velocity field \( v(z,t) \) but different fibres followed by analysis of the ensemble average \( \langle A(z) \rangle \). For Rayleigh scattering, eq. (A.4) simplifies to

\[
\langle A_{\text{DAS}}(z) \rangle = S_0^2(z) * [v(z) - v(z - L_0)],
\]

(A.5)

To illustrate the effect of random fibre reflectivity, simulated numerically the DAS response corresponding to the movement of a 40m segment of fibre (no deformation occurs inside the segment), for \( \tau = 10—100\text{ns} \) and the gauge length \( L_0 = 10\text{m} \) (fig. A.9). If the pulse width is small, agreement with the theory is good. But for a typical pulse width, this effect causes significant errors in estimates of the velocity field \( v(z) \).

This observation explains a general approach to choosing the pulse width.
Figure A.8: A schematic illustration of the main principle behind the distributed acoustic measurements. A finite monochromatic laser pulse $s(t')$ reflects back continuously along the fibre, but at the moving point the reflected pulse $s_2$ also gains a time-dependent phase shift, which may be perceived as a Doppler frequency shift $\pm \Omega$ (the sign changes depending on whether $z < z_0$ or $z > z_0$). In a two-armed interferometer with a delay line of the length $2L_0$, $s_2$ interferes first with a reflection $s_1$ passed through the delay line, and then $s_2$ passed through the delay line interferes with $s_3$ coming out of the straight line. For the both interferences, photon counts in the photodetector feature beating at the Doppler frequency $\Omega$. A strain analyser is a conceptual instrument that extracts the magnitude and sign of the beating of $\frac{\partial I(t)}{\partial t}$. 
On one hand, a longer pulse smooths out the instrumentation noise, but if a pulse is too long it becomes very sensitive to the inhomogeneities within the fibre. A compromise between the two considerations is usually achieved by choosing $L_0 = 2\tau$. It is worth noting that the above simulation was carried out in the absence of noise. The fluctuations (fig. A.9) can be even more drastic when reflected light disappears for some distances. Such flicker noise can be suppressed partially by weighted averaging, but it is still a problem for DAS with a conventional fiber.

We can increase SNR and reduce the distortions simultaneously by using an engineered fiber with regularly spaced high reflectivity markers. With $L_0 = 2\tau$, such a design prevents an overlap between the reflected pulses and minimises the effects of fluctuations of the fibre reflectivity. This idea is implemented in iDASv3™ system. The reflectivity of the engineered fibre becomes

$$r(z) = R \cdot \sum_j \delta(z - jL_0) = R \cdot \text{comb}(z/\tau),$$  \hspace{1cm} (A.6) $$

where $\text{comb}(\cdot)$ is a comb function, also known as a sampling operator. DAS
response for the engineered fiber $A_E(z)$ from eq. (A.4) becomes

$$A_E(z) = R^2 \sum_j [v([j + 1]L_0) - v(jL_0)] \tau^2(z - jL_0).$$  \hspace{1cm} (A.7)

Then, the DAS output for the engineered fiber can be rearranged to a form similar to eq. (A.6),

$$A_E(z) = s_0^2(z) \ast \{[v(z) - v(z - L_0)]\text{comb}(a/\tau)\}.$$  \hspace{1cm} (A.8)

For the engineered fibre, effect of fluctuations of refraction index on the DAS response is negligible, and hence the ensemble averaging becomes unnecessary.

In Fourier domain with a spatial frequency $k_z$, the spectrum of the DAS response from eqs. (A.7) and (A.8), $F_E(k_z)$, can be expressed via the spatial spectrum of the displacement velocity field along the fibre $F_v(k_z)$ as

$$F_E(k_z) = F_{\text{DAS}} \ast \left[ \text{comb}(k_z\tau/2\pi) \ast F_v(k_z) \right],$$  \hspace{1cm} (A.9)

where we assumed that the pulse is a unit rectangular function. The DAS receiver function $F_{\text{DAS}}$ is

$$F_{\text{DAS}}(k_z) = \omega \cdot |\text{sinc}(k_z\tau/2) \cdot \sin(k_zL_0/2)|.$$  \hspace{1cm} (A.10)

Because $v = \frac{\partial u(t)}{\partial t}$, conversion of the DAS measurements to displacements will feature also a factor $\omega$ (see [1]).

We can conclude that, unlike DAS with a conventional fibre, the spectrum of the DAS response with an engineered fiber is subjected to aliasing similar to an array of geophones. Figure A.10 shows the spectra $F_{\text{DAS}}$ for typical parameters of DAS measurements. Clearly, an engineered fibre may be used until the cut-off frequency if an appropriate anti-aliasing filter is deployed, while a conventional fibre has no distortions in a wider frequency range, but its sensitivity drops with increasing frequency.

Design of the engineered fiber dictates the gauge length. However, it is possible to synthesise a long optical gauge length by shifting and stacking the measurements obtained with a short gauge length, as follows from eq. (A.8). In
this case, the low-frequency response improves significantly, although the spatial bandwidth shrinks (see the line for long gauge length $L_0 = 30\text{m}$ in fig. A.10).

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