Textual Description for Mathematical Equations

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Abstract—Reading of mathematical expression or equation in the document images is very challenging due to the large variability of mathematical symbols and expressions. In this paper, we pose reading of mathematical equation as a task of generation of the textual description which interprets the internal meaning of this equation. Inspired by the natural image captioning problem in computer vision, we present a mathematical equation description (MED) model, a novel end-to-end trainable deep neural network based approach that learns to generate a textual description for reading mathematical equation images. Our MED model consists of a convolution neural network as an encoder that extracts features of input mathematical equation images and a recurrent neural network with attention mechanism which generates description related to the input mathematical equation images. Due to the unavailability of mathematical equation image data sets with their textual descriptions, we generate two data sets for experimental purpose. To validate the effectiveness of our MED model, we conduct a real-world experiment to see whether the students are able to write equations by only reading or listening their textual descriptions or not. Experiments conclude that the students are able to write most of the equations correctly by reading their textual descriptions only.

Keywords—Mathematical symbols; mathematical expressions; mathematical equation description; document image; convolution neural network; attention; recurrent neural network.

I. INTRODUCTION

Learning of mathematics is necessary for students at every stage of student life. Solving mathematical problems is an alternative way to develop and improve their mathematical skills. Unfortunately, blind and visually impaired (VI) students face the difficulties to especially learn mathematics due to their limitations in reading and writing mathematical formulas. In generally, human readers help those categories of students to access and interpret materials or documents of mathematics courses. However, at every time, it is impossible and impractical for those categories of students having human reader; because of the cost and the limited availability of the trained personnel. Braille is the popular and more convenient way to access the document for blind and VI students. Unfortunately, many documents are not available in Braille, since the conversion of mathematical documents in Braille is more difficult and complicated [1]. Moreover, it is also difficult for students who are comfortable for reading literary Braille transcriptions [2].

Other than Braille, sound based representation of documents is also an important and popular way to access information for those kinds of students. In this direction, DAISY books and talking books are commonly used audio materials for understanding documents. However, these books are less prepared for mathematical expressions or equations (MEs) [2]. Recently, text-to-speech (TTS) systems have been widely used by blind and VI students to read electronic text through computers. TTS systems convert digital text into synthetic speech. Unfortunately, most available TTS systems can read only plain text. They fail to generate appropriate speech when it comes across mathematical equations.

Many researchers realized that it is very important to enhance the accessibility of mathematical materials to the blind and VI students and developed TTS based mathematical expressions reading systems [3]–[5]. Some of these developed systems need extra words to read an ME. Due to the extra words, the rendered audio is very long. Hence, the students may not always be able to interpret the main point of the expressions due to long audio duration. Moreover, most of these existing automatic math reading systems take MEs as input in the form of LaTeX or other similar markup languages. Unfortunately, all available mathematical documents are not in the form of LaTeX or any other markup language. Therefore, generation of LaTeX or other markup languages corresponds to mathematical documents is also challenging [2].

In this paper, our goal is to develop a framework, called as mathematical equation description (MED) model which can help the blind and VI students for reading/interpreting internal meaning of MEs present in the document images. We pose reading of ME as a problem of generation of natural language description. Basically, our proposed MED model automatically generates textual (natural language) description which can able to interpret the internal meaning of the ME. For examples, \( \int \sin x \, dx \) is a ME and its textual description is like “integration of \( \sin x \) with respect to \( x \).
With the textual description, the blind and VI students can easily read/interpret the MEs. Figure 1 shows the generated textual description of an MEI using our MED model. This task is closely related to image description/captioning task [6]. However, description of equation is very sensitive with respect to variables, operators and their positions. Figure 2 illustrates the sensitivity of variables, operators and their positions during generation of textual description task. For example, $3x$ in Figure 2(a), it can be read as “three times x”. While 3 is changing its position e.g. $3^x$ in Figure 2(c), textual sentence “x power of three” for reading, it is totally different from previous equation. As per our understanding goes, this is the first work where reading/interpreting of MEs is posed as a generation of textual description task.

The main inspiration of our work comes from image captioning, a recent advancement in computer vision. In this paper, we propose an end-to-end trainable deep network to generate natural language descriptions for the MEs which can read/interpret the internal meaning of these expressions. The network consists of two modules: encoder and decoder. The encoder encodes the ME images using Convolution Neural Networks (CNNs). Long Short Term Memory (LSTM) network as decoder that takes the intermediate representation to generate textual descriptions of corresponding ME images. The attention mechanism impels the decoder to focus on specific parts of the input image. The encoder, decoder and attention mechanism are trained in a joint manner. We refer this network as Mathematical Equation Description (MED) network.

In particular, our contributions are as follows.

- We present an end-to-end trainable deep network with the combination of both vision and language models to generate description of MEs for reading/interpreting MEs.
- We generate two data sets with ME images and their corresponding natural language descriptions for our experimental purpose.
- We conduct a real world experiment to establish effectiveness of the MED model for reading/interpreting mathematical equation.

II. RELATED WORK

A. Mathematical Expression Recognition

Automatic recognition of MEs is one of the major tasks towards transcribing documents into digital form in the scientific and engineering fields. This task mainly consists of two major steps: symbol recognition and structural analysis [7]. In case of symbols recognition, the initial task is to segment the symbols and then to recognize the segmented symbols. Finally, structural analysis of the recognized symbols have been done to recognize the mathematical expressions. These two problems can be solved either sequentially [8] or a single framework (global) [9]. However, both of these sequential and global approaches have several limitations including (i) segmentation of mathematical symbols is challenging for both printed and handwritten documents as it contains a mix of text, expressions and figures; (ii) symbols recognition is difficult because a large number of symbols, fonts, typefaces and font sizes [7]; (iii) for structural analysis, commonly two dimensional context free grammar is used which requires prior knowledge to define math grammar [10] and (iv) the complexity of parsing algorithm increases with the size of math grammar [11].

Due to the success of deep neural network in computer vision task, the researchers adopted deep neural models to recognize mathematical symbols [12], [13] and expressions [14]–[18]. In [12], [13], the authors considered CNN along with bidirectional LSTM to recognize mathematical symbols. Whereas, [14], [15] explored the use of attention based image-to-text models for generating structured markup for MEs. These models consist of a multi-layer convolution
network to extract image features with an attention based recurrent neural network as a decoder for generating structured markup text. In the same direction, Zhang et al. [18] proposed a novel end-to-end approach based on neural network that learns to recognize handwritten mathematical expressions (HEMs) in a two-dimensional layout and produces output as one-dimensional character sequences in the LaTeX format. Here, the CNN, as encoder is considered to extract feature from HEM images and a recurrent neural network is employed as decoder to generate LaTeX sequences.

B. Image Captioning

Image captioning is a task which automatically describes the content of an image using properly formed English sentences. Although, it is a very challenging task, it helps the visually impaired people to better understand the content of images on the web. Recently, a large variety of deep models [6], [19]–[22] have been proposed to generate textual description of natural images. All these models considered recurrent neural network (RNN) as language models conditioned on the image features extracted by convolution neural networks and sample from them to generate text. Instead of generating caption for whole image, a handful of approaches to generate captions for image regions [6], [23], [24]. In contrast of generating a sentence, various models have also been introduced to generate paragraph for describing content of the images in literature [25], [26] by considering a hierarchy of language models.

III. MATHEMATICAL EQUATION DESCRIPTION

A. Overview

Our MED model takes a mathematical expression image (MEI) as an input and generates a natural language sentence to describe the internal meaning of this expression. Figure 3 provides an overview of our model. It consists of encoder and decoder networks. The encoder extracts deep features to richly represent the equation images. The decoder uses the intermediate representation to generate a sentence to describe the meaning of the ME. The attention mechanism impels the decoder to focus on specific parts of the input image. Each of these networks are discussed in details in the following subsections.

B. Feature Extraction using Encoder

The MED model takes a MEI and generates its textual description $Y$ encoded as a sequence of 1-of-$K$ encoded words.

$$Y = \{y_1, y_2, ..., y_T\}, \quad y_i \in \mathbb{R}^K \quad (1)$$

where $K$ is the size of the vocabulary and $T$ is the length of the description. We consider a Convolution Neural Network (CNN) as an encoder in order to extract a set of feature vectors. We assume that the output of CNN encoder is a three-dimensional array of size $H \times W \times D$, and consider the output as a variable length grid of $L$ vectors, $L = H \times W$ as referred to annotation vectors. Each of these vector is $D$-dimensional representation that corresponds to a local region of the input image.

$$A = \{a_1, a_2, ..., a_L\}, \quad a_i \in \mathbb{R}^D \quad (2)$$

We extract features from a lower convolution layer in order to obtain a correspondence between the feature vectors and regions of the image. This allows the decoder to selectively focus on certain regions of the input image by selecting a subset of all these feature vectors.

C. Sentence Generation using Decoder

We employ LSTM [27] as a decoder that produces a sentence by generating one word at every time step conditioned on a context vector $\hat{z}_t$, the hidden state $h_t$ and the previously generated word $y_{t-1}$. It produces word at time step $t$ using the following equation:

$$p(y_t|y_1, y_2, ..., y_{t-1}, x) = f(y_{t-1}, h_t, \hat{z}_t), \quad (3)$$

where $x$ denotes the input MEI and $f$ denotes a multi-layered perceptron (MLP) which is expanded in Eq. (7). The hidden state $h_t$ of LSTM is computed using following equation:

![Figure 3: Overview of mathematical expression description network. Our model uses an end-to-end trainable network consisting of CNN followed by a language generating LSTM. It generates textual description of an input mathematical expression image in natural language which interprets its internal meaning.](image-url)
\[ i_t = \sigma(W_{yi}E_{y_{t-1}} + U_{hi}h_{t-1} + V_{zi}\tilde{z}_t) \]
\[ f_t = \sigma(W_{yi}E_{y_{t-1}} + U_{hi}h_{t-1} + V_{zf}\tilde{z}_t) \]
\[ o_t = \sigma(W_{yi}E_{y_{t-1}} + U_{ho}h_{t-1} + V_{zo}\tilde{z}_t) \]
\[ g_t = \tanh((W_{yi}E_{y_{t-1}} + U_{ho}h_{t-1} + V_{zc}\tilde{z}_t)) \]
\[ c_t = f_t \odot c_{t-1} + i_t \odot g_t \]
\[ h_t = o_t \odot \tanh(c_t). \]

Here, \( i_t, f_t, c_t, o_t \) and \( h_t \) are the input, forget, memory, output and hidden states of the LSTM, respectively. The vector \( \tilde{z}_t \) is a context vector which captures visual information of a particular image region. The context vector \( \tilde{z}_t \) (in Eq. (4)) is a dynamic representation of the relevant part of the input image at time step \( t \). We consider soft attention defined by Bahdanau et al. [28] which computes weight \( \alpha_{ti} \) of each annotation vectors \( a_i \) conditioned on the previous LSTM hidden state \( h_{t-1} \). Here, we parameterize attention as MLP which is jointly trained:

\[ e_{ti} = v_a^T \tanh(W_a h_t + U_a a_i) \]
\[ \alpha_{ti} = \frac{\exp(e_{ti})}{\sum_{k=1}^{K} \exp(e_{tk})}. \]  

Let \( n \) be the dimension of the attention, then \( v_a \in \mathbb{R}^{n \times n} \), \( U_a \in \mathbb{R}^{n \times D} \). After computation of the weights \( \alpha_{ti} \), the context vector \( \tilde{z}_t \) is calculated as follows:

\[ \tilde{z}_t = \sum_{i=1}^{L} \alpha_{ti} a_i. \]

This weight \( \alpha_{ti} \) will make decoder to know which part of input image is the suitable place to attend to generate the next predicted word and then assign a higher weight to the corresponding annotation vectors \( a_i \). \( m \) and \( n \) denote the dimensions of embedding and LSTM, respectively; \( E \in \mathbb{R}^{m \times K} \) is the embedding matrix. \( \sigma \) is sigmoid activation function and \( \odot \) is element wise multiplication.

Finally, the probability of each predicted word at time \( t \) is computed by the context vector \( \tilde{z}_t \), current LSTM hidden state \( h_t \) and previous predicted word \( y_{t-1} \) using the following equation:

\[ p(y_t | y_1, y_2, ..., y_{t-1}, x) = g(W_o(E_{y_{t-1}} + W_h h_t + W_z \tilde{z}_t)), \]

where \( g \) denotes a softmax activation function over all the words in the vocabulary; \( E, W_o \in \mathbb{R}^{K \times n}, W_h \in \mathbb{R}^{m \times n} \) and \( W_z \in \mathbb{R}^{m \times D} \) are learned parameters initialized randomly.

The initial memory state \( c_0 \) and hidden state \( h_0 \) of the LSTM are predicted by an average of the annotation vectors fed through two separate MLPs \((f_{init}, c, f_{init}, h)\):

\[ c_0 = f_{init}, c \left( \frac{1}{L} \sum_{i=1}^{L} a_i \right) \]
\[ h_0 = f_{init}, h \left( \frac{1}{L} \sum_{i=1}^{L} a_i \right). \]

| Expression | Description |
|------------|-------------|
| \( x^2 \) | ten times \( x \) |
| \( \sqrt{x} \) | second root of \( x \) |
| \( \frac{1}{x} \) | \( x \) over ten |
| \( (x + y)^2 \) | second power of all \( x \) plus \( y \) |
| \( \log_2 x \) | \( x \) over two |
| \( \frac{y}{x} \) | \( x \) over \( y \) plus \( z \) |
| \( \frac{y^2}{x^2} \) | \( x \) plus \( y \) all over \( z \) |
| \( \frac{(y + z)}{x} \) | \( x \) over \( y \) square |
| \( x + y \) | \( x \) all plus \( y \) over \( z \) |
| \( x - y \) | \( x \) minus \( y \) all over \( z \) plus \( z \) |
| \( x + y \) | \( x \) plus \( y \) over \( z \) |
| \( x^2 \) | \( x \) square over \( y \) |
| \( x - y \) | \( x \) minus \( y \) all over \( z \) plus \( t \) |
| \( x + y \) | \( x \) plus \( y \) all over \( z \) plus \( t \) |
| \( e^{(1+x)} \) | exponential of all one plus \( x \) |
| \( e^{(1+z)} \) | exponential of all one plus \( z \) |
| \( \int x \, dx \) | integral of \( x \) with respect to \( x \) |
| \( \int_0^1 x \, dx \) | integral of \( x \) with respect to \( x \) from lower limit \( 0 \) to \( 1 \) |
| \( \lim_{x \to \infty} \frac{\sin x}{x} \) | limit of \( \sin x \) over \( x \) as \( x \) approaches to zero |
| \( \frac{d}{dx}(x^2) \) | differentiation of \( x \) square with respect to \( x \) |
| \( 2x - 6 = 3 \) | \( x \) minus six equal to three |
| \( x + 7 > 10 \) | \( x \) plus seven greater than ten |
| \( x + 2y = 7 \) | \( x \) plus two times \( y \) equal to seven and |
| \( x - y = 3 \) | \( x \) minus \( y \) equal to three |

**Table I:** Natural language phrases to uniquely describe mathematical equations.

**D. Implementation Details**

**Pre-processing:** Textual descriptions of the MESs are pre-processed with basic tokenization algorithm by keeping all words that appeared at least 4 times in the training set.

**Training Details:** The training objective of our MED model is to maximize the predicted word probability as given in Eq. (7). We use cross entropy as the objective function:

\[ O = - \sum_{t=1}^{T} \log p(y^g | y_t, x), \]

where \( y^g \) represents the ground truth word at time step \( t \).

We consider 299K images and their corresponding textual descriptions to train the model. We consider pre-trained ResNet-152 model [29] (on ImageNet [30]). We do this in all the experiments. We train the network with batch size of 50 for 60 epochs. We use stochastic gradient descent (SGD) with fixed learning rate \( 10^{-4} \), momentum = 0.5 and weight decay = 0.0001. All the weights were randomly initialized except for the CNN. We use 512 dimensions for the embedding and 1024 for the size of the LSTM memory. We consider a dropout layer after each convolution layer and set as 0.5. The best trained model is determined in terms of BLEU-4 score on validation set. For further implementation and architecture details, please refer to the source code at: https://github.com/ajoymondal/Equation-Description-PyTorch.
Decoding: In decoding stage, our main aim is to generate a most likely textual description for a given MEI:

\[ \hat{y} = \arg \max_y \log p(y|x). \quad (10) \]

Different from training procedure, the ground truth of previous predicted word is not available. We employ beam search [31] of size 20 during decoding procedure. A set of 20 partial hypothesis beginning with the start-of-sentence <start> is maintained. At each time step, each partial hypothesis in the beam is expanded with every possible word. Only the 20 most likely beams are kept. When the <start> token is encounter, it is removed from the beam and added to the set of complete hypothesis. This process is repeated until the output word becomes a symbol corresponding to the end-of-sentence <end>.

IV. DATA SETS AND EVALUATION METRICS

A. Data Sets

Unavailability of mathematical equation image data sets and their textual descriptions inspired us to generate data sets for experimental purpose. Various issues must be concerned during generation of unambiguous textual description of a mathematical equation. One important issue is that the same textual description can lead to the different expressions. For example, the textual description like “\( x + \frac{y}{2} \)” could be description of two possible equations: either \( x + \frac{z}{2} \) or \( x + \frac{z}{2} \). Thus, an algorithm should be carefully designed to generate an unambiguous textual description corresponds to exactly one expression. As far as our knowledge goes, no mathematical expression data sets with their textual descriptions is available for experiment. We create a data set, referred as Math-Exp-Syn with large number of synthetically generated MEIs and their descriptions. For this purpose, we create sets of predefined functions (e.g. linear equation, limit, etc.), variables (e.g. \( x, y, z \), etc.), operators (e.g. +, −, etc.) and constants (e.g. 10, 1, etc.) and sets of their corresponding textual descriptions. We develop a python code which randomly selects a function, variable, operator and constant from the corresponding predefined sets and automatically generates mathematical equation as an image and corresponding textual description in the text format. We make our Math-Exp-Syn data generation code available at: https://github.com/ajoymondal/Equation-Description-PyTorch. We also create another data set, referred as Math-Exp by manually annotating a limited number of MEIs. During creation of both these data sets, we take care the uniqueness of the equations and their descriptions. We consider the following natural language sentences listed in table I to uniquely describe the internal meaning of the equations.

In this work, we limit ourselves to only seven categories of MES: linear equation, inequality, pair of linear equations, limit, differentiation, integral and finite integral. Table II displays the category wise statistics of these data sets. Figure 4 shows few sample images and their descriptions of Math-Exp-Syn data set.

B. Evaluation Metrics

In this work, we evaluate the generated descriptions for MEI with respect to three metrics: BLEU [32], CIDEr [33], and ROUGE [34] which are popularly used in natural language processing (NLP) and image captioning tasks. All these metrics basically measure the similarity of a generated sentence against a set of ground truth sentences written by humans. Higher values of all these metrics indicate that the generated sentence (text) is more similar to the ground truth sentence (text).

V. EXPERIMENTS AND RESULTS

An extensive set of experiments is performed to assess the effectiveness of our MED model using several metrics on the ME data sets.

| Data set       | Division      | No. images | Total |
|----------------|---------------|------------|-------|
| Math-Exp-Syn   | Training      | 1K 3K       | 4K K  |
|                | Validation    | 5K 5K 6K   | 11K 11K|
|                | Test          | 5K 5K 6K   | 15K 15K|
| Math-Exp       | Test          | 1K 0.64K 0.6K | 1K 2.6K|
Figure 5: Visual illustration of sample results of test Math-Exp-Syn data set produced by our MED framework. GT: ground truth description, OP1: description generated by ResNet152+LSTM, OP2: description generated by ResNet152†+LSTM and Attn., OP3: description generated by ResNet152†+LSTM+Attn., OP4: description generated by ResNet152†+GRU+Attn., RNN: description generated by ResNet152†+RNN+Attn., † indicates fine-tune and Attn. denotes attention in decoder. Red colored text indicates wrongly generated text.

A. Ablation Study

A number of ablation experiments is conducted to quantify the importance of each of the components of our algorithm and to justify various design issues in the context of mathematical equation description. Math-Exp-Syn data set is used for this purpose.

Table III: It illustrates that the deeper pre-trained model gets better representation and improves textual description accuracy with respect to three evaluation measures: BLEU-1 (B-1), BLEU-2 (B-2), BLEU-3 (B-3), BLEU-4 (B-4), CIDER (C) and ROUGE (R). Number along with the model refers to the depth of the corresponding model. † indicates fine-tune and Attn. denotes attention in decoder. LSTM with attention is considered as a decoder.

Pre-trained Encoder: It is well known that the deeper networks are beneficial for the large scale image classification task. We conduct an experiment with different depths of the pre-trained models to analyze their performances on the mathematical equation description task. Detailed scores of equation description using the various pre-trained models are listed in Table III.

Table IV: Quantitative illustration of effectiveness of fine-tuning the encoder and attention in decoder during training on MED task. † indicates fine-tune.

Pre-trained Encoder vs. Without Fine-tuned Encoder and Attention vs. Without Attention in Decoder: The considered encoder, ResNet152 pre-trained on ImageNet [30] is not effective without fine-tuning due to domain heterogeneity (natural images and MATH). We perform an experiment to establish potency of fine-tuning on the equation description.
task. The attention mechanism tells the decoder to focus on a particular region of the image while generating the description related to that region of the image. We do an experiment to analyze the effectiveness of attention mechanism on the mathematical equation description task. Observation of the experiments is quantitatively reported in Table IV. This table highlights the effectiveness of fine-tuning the pre-trained ResNet-152 and LSTM with attention for MED task.

RNN vs. GRU vs. LSTM: We also conduct an experiment to analyze performances of LSTM, Gated Recurrent Units (GRU) and Recurrent Neural Networks (RNN) on generating captions for mathematical equation images. In this experiment, we consider pre-trained ResNet-152 as an encoder which is fine-tuned during training and different decoders: RNN, GRU and LSTM with attention mechanism. Table V displays the numerical comparison between three decoder models. The table highlights that LSTM is more effective than other two models for mathematical equation description task. Second and third rows of Figures 5 display the visual outputs. This figure highlights that LSTM is able to generate text most similar to the ground truth.

Table V: Performance comparison between RNN, GRU and LSTM with attention mechanism on the mathematical equation description task. We fine-tune the encoder during training process.

| Models                  | Test Performance | B-1 | B-2 | B-3 | B-4 | C | R |
|-------------------------|------------------|-----|-----|-----|-----|---|---|
| ResNet-152†+RNN+Attn.  |                  | 0.977 | 0.958 | 0.939 | 0.920 | 0.967 | 9.179 |
| ResNet-152†+GRU+Attn.  |                  | 0.979 | 0.959 | 0.939 | 0.920 | 0.968 | 9.182 |
| ResNet-152†+LSTM+Attn. |                  | 0.981 | 0.962 | 0.941 | 0.923 | 0.971 | 9.184 |

Table VI: Quantitative results of our MED model on standard evaluation metrics for both Math-Exp-Syn and Math-Exp data sets. Both the cases MED is trained using training set of Math-Exp-Syn data set.

| Models | Data sets       | Division | Scores | B-1 | B-2 | B-3 | B-4 | C | R |
|--------|----------------|----------|--------|-----|-----|-----|-----|---|---|
| MED    | Math-Exp-Syn   | test set |        | 0.981 | 0.962 | 0.941 | 0.923 | 0.971 | 9.184 |
| MED    | Math-Exp       | test set |        | 0.975 | 0.956 | 0.936 | 0.917 | 0.966 | 9.146 |

B. Quantitative Analysis of Results

The quantitative results obtained using our MED model for both Math-Exp-Syn and Math-Exp data sets are listed in Table VI.

C. Real world Experiments

We conduct a real world experiment to see whether the students are able to write the equations by only reading or listening their textual descriptions or not. For this purpose, we create a test set of mathematical equation images which are cropped from NCERT class V mathematical book\(^1\). Test set consists of 398 cropped equation images of various types of equations: integer, decimal, fraction, addition, subtraction, multiplication and division. Figure 6 shows the sample cropped mathematical equation images from NCERT class V mathematical book. Our MED system generates the textual description for each of these equations. The list of descriptions of equations is given to the students and ask them to write corresponding equations by reading the descriptions. Third Column: equations written by the students.

Table VII: Summary of real world experiments. First Column: cropped equation images. Second Column: textual descriptions generated by the MED and given to the students and ask them to write corresponding equations by reading the descriptions. Third Column: equations written by the students.

\(1\)https://www.ncertbooks.guru/ncert-maths-books/
wrongly generated descriptions. From this test, we conclude that our MED model is effective for reading equations by generating their textual descriptions.

VI. CONCLUSIONS

In this paper, we introduce a novel mathematical equation description (MED) model for reading mathematical equations for blind and visually impaired students by generating textual descriptions of the equations. Unavailability of mathematical images and their textual descriptions, inspires us to generate two data sets for experiments. Real-world experiment concludes that the students are able to write mathematical expression by reading or listening their descriptions generated by the MED network. This experiment establishes the effectiveness of the MED framework for reading mathematical equation for the blind and VI students.

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