Pinning Action of Correlated Disorder against Equilibrium Properties of HgBa$_2$Ca$_2$Cu$_3$O$_x$: a Delicate Balance

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We report significant alteration of the equilibrium properties of the superconductor HgBa$_2$Ca$_2$Cu$_3$O$_x$ when correlated disorder in the form of randomly oriented columnar tracks is introduced via induced fission of Hg-nuclei. From studies of the equilibrium magnetization $M_{eq}$ and the persistent current density over a wide range of temperatures, applied magnetic fields, and track densities up to a “matching field” of 3.4 Tesla, we observe that the addition of more columnar tracks acting as pinning centers is progressively offset by reductions in the magnitude of $M_{eq}$. Invoking anisotropy induced “refocusing” of the random track array and incorporating vortex-defect interactions, we find that this corresponds to increases in the London penetration depth $\lambda$; this reduces the vortex line energy and consequently reduces the pinning effectiveness of the tracks.

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I. INTRODUCTION

Much has been done over the past decade or so to understand the interaction of superconducting vortices in high $T_c$ cuprates with correlated disorder, which generally gives strong vortex pinning. Most widely studied have been columnar defects, which typically are formed by irradiation with energetic heavy ions; such particles are highly ionizing and create tracks of amorphous material along their path. Many morphologies have been investigated, ranging from the familiar parallel tracks to inclined defects, crossed arrays with “designer splay,” etc. Early theoretical insights and ideas came from Nelson and Vinokur and Hwa et al. Numerous experimental studies have shown that such defects are supremely efficient in localizing vortices to their vicinity. This is manifest through strong enhancements of critical ($J_c$) and persistent current densities in some regions of the phase space. It is also clear that outside these confined regions the localization effects are lessened, in part by the complex vortex (variable range hopping) dynamics which interferes and competes with pinning.

Vortex pinning by proton-generated fission defects was first demonstrated in Bi-cuprate materials and can be generally applied in cuprate superconductors that contain a sufficient density of heavy nuclei. The method was devised to circumvent a problem of generating CD’s by heavy ion irradiation, namely their limited range, typically a few tens of micrometers. Krusin-Elbaum et al. demonstrated an indirect formation of columnar defects by irradiation with deeply penetrating 0.8 GeV protons. An incident proton is absorbed by a heavy nucleus (Hg in the present case) in the material, excites it, and induces it to fission into two particles with similar mass. The recoiling fission fragments, each having $\sim$ 100 MeV energy, form randomly oriented columnar defects (CD’s) deep within the superconductor. In a different approach, Weinstein and coworkers created CD’s by doping a superconductor with $^{235}$U, which is induced to fission by irradiation with thermal neutrons. High-$T_c$ materials containing randomly oriented CD’s exhibit a variety of interesting physical phenomena, e.g., a temperature-independent quantum tunneling of vortices in Bi-2212 materials. In studies of Hg-cuprates containing 1, 2, and 3 adjacent CuO layers, it was shown that sufficiently high superconductive anisotropy can lead to a rescaling of the splayed landscape of random CD’s. As a consequence, the pinning array and the applied field are “refocused” toward the crystalline c-axis, even in polycrystalline materials. Later we use this feature for interpreting the present studies.

In addition to providing vortex pinning sites, correlated disorder doubtless also affects the equilibrium superconducting properties, e.g., the characteristic length scales such as $\lambda$ and $\xi$. What is little known, however, is how this alters the pinning landscape; for example, an increase in $\lambda$ will reduce the vortex line energy and hence the pinning force will be reduced.

In this work, we examine the equilibrium magnetization $M_{eq}$ in the mixed state of the anisotropic cuprate HgBa$_2$Ca$_2$Cu$_3$O$_x$, both in its virgin state and when containing randomly splayed columnar defects installed by fission. For virgin Hg-1223, the $M_{eq}$ can be scaled, following a recent formulation. With the addition of splayed CD’s, the magnitude of $M_{eq}$ decreases significantly, especially at low fields. In addition, the defects generate a pronounced deviation from the ‘standard’ London field dependence, giving an anomalous “S” shape to plots of $M_{eq}$ versus ln($H$). By using the concept that sufficiently large anisotropy rescales the ran-
dom track collection into an equivalent parallel defect array we apply—in addition to a conventional London description—the vortex-defect interaction model by Wahl et al. which considers a Poisson distribution of parallel tracks. We show that the “S” shape of $M(T)$ is accounted for by the magnetic coupling between defects and vortices. The London penetration depth $\lambda$ significantly and progressively increases, in accordance with the Wahl-Buzdin description. This effect counteracts the nominally positive influence of increasing the defect density $B_\Phi$ and it plays a major role in determining the level of $B_\Phi$ that maximizes the current density $J_c$.

II. EXPERIMENTAL ASPECTS

Samples for study were bulk polycrystalline HgBa$_2$Ca$_2$Cu$_3$O$_x$ materials (Hg-1223) containing sets of 3 adjacent oxygen-copper layers. Small pieces, typically 30 mg mass and $\sim 1$ millimeter thickness, were all cut from the same pellet. The samples were irradiated at room temperature in air with 0.8 GeV protons at the Los Alamos National Laboratory. Proton fluences $\phi_p$ were 0, 1.0, 3.2, 10, 19, and $35 \times 10^{16}$ protons/cm$^2$, as determined from the activation of Al dosimetry foils. The resulting density of fission events is $N/V = \phi_p \sigma_f n_{Hg}$. Here $n_{Hg}$ is the number density of Hg nuclei and $\sigma_f \approx 80$ millibarns is the cross-section for inducing a prompt fission of Hg nuclei. Each fission produces one CD, so $N/V$ is the volume density of defects, also. One can convert this into an approximate area density of CD’s by multiplying by the track length $\sim 8$ $\mu$m, and the area density can be reexpressed in units of a matching field $B_\Phi$ by multiplying by the flux quantum $\Phi_0$. Resulting values for the defect density are $B_\Phi = 0, 0.1, 0.3, 1.0, 1.9,$ and 3.4 Tesla, respectively. The fission process is random in direction, giving randomly oriented CD’s. Transmission electron microscopy (TEM) studies of both Bi-2212 and Hg-cuprates have demonstrated the presence of randomly oriented columnar defects in these high-$T_c$ materials.

The superconductive properties of the virgin and processed samples were investigated magnetically. A SQUID-based magnetometer (model Quantum Design MPMS–7), equipped with a high homogeneity 7 T superconductive magnet, was used for studies in the temperature range 5–295 K, in applied fields to 6.5 T. The superconductive transition temperatures $T_c$ were measured in an applied field of 4 Oe (0.4 mT) in zero-field-cooling (ZFC) and field-cooling (FC) modes. The resulting values for the onset temperature $T_c$ are 133, 134, 132.3, 132, 131, and 129.3 K, respectively. Values for the Meissner (FC) fraction $-4\pi M/H$ lie in the range of 40–50%, except at the highest fluence where the fractional flux expulsion was 29%.

The isothermal magnetization $M$ was measured as a function of applied magnetic field. Below $T_c$, and below the irreversibility line, the magnetization was hysteretic due to the presence of intragrain persistent currents. From the magnetic irreversibility $\Delta M = [M(H \downarrow) - M(H \uparrow)]$, the persistent current density $J$ was obtained using the Bean critical state relation $J \propto \Delta M/r$, where $r \approx 4$ $\mu$m is the mean grain radius. Measurements of the background magnetization in the normal state above $T_c$ were used to correct the data in the superconducting state, in order to obtain the equilibrium magnetization $M_{eq}$. Above the irreversibility line where $\Delta M = 0$, this process yields $M_{eq}$ directly; near the irreversibility line where $\Delta M$ is small, we obtain $M_{eq}$ from the (background-corrected) average magnetization $[M(H \downarrow) + M(H \uparrow)]/2$, as illustrated in the next section.

III. EXPERIMENTAL RESULTS

A. Equilibrium Properties of Virgin Hg-1223

We begin by considering the equilibrium magnetization in the mixed state. Figure 1 illustrates the method used to obtain $M_{eq}$ by plotting the background-corrected experimental magnetization for the virgin material (open squares) versus applied magnetic field $\mu_0 H$ on a logarithmic scale. As described above, the closed symbols show the average $M$, which provides a very good approximation to $M_{eq}$ when the hysteresis is small. The solid line is a fit to conventional London theory, which provides that $M_{eq}$ is directly proportional to $(1/\lambda_{ab}) \times \ln(\beta H_{c2}/H)$, where $\lambda_{ab}$ is the in-plane London penetration depth, $\beta \approx 1.4$ is a constant of order unity, and $H_{c2}$ is the upper critical field. More explicitly, one has with $H \parallel c$-axis of a uniaxial superconductor that

$$M_{eq} = - (\Phi_0/32\pi^2 \lambda_{ab}^2) \times \ln(\beta H_{c2}/H)$$

If $H$ is oriented at angle $\theta$ with respect to the $c$-axis, the resulting response can be obtained from the anisotropy function

$$\varepsilon(\theta) = \{\cos^2(\theta) + (1/\gamma^2) \sin^2(\theta)\}^{1/2}$$

where $\gamma = (m_c/m_{ab})^{1/2}$ is the mass anisotropy ratio. For a randomly oriented polycrystalline material, the angularly averaged equilibrium magnetization is

$$\langle M_{eq} \rangle = - (\Phi_0/32\pi^2 \lambda_{ab}^2) \times \left[(1/2) \ln(\beta H_{c2}/H) + (1/4)\right]$$

in the limit that $\gamma$ is large.

The straight line fit in Fig. 1 shows that the London $\ln(H)$ logarithmic variation describes the field dependence well. Also shown for immediate qualitative comparison are data for $M_{eq}$ of irradiated samples (at 77 K) with defect densities $B_\Phi \approx 1.0$ and 3.4 T.

Results for $M_{eq}$ in the virgin Hg-1223 material at other temperatures are presented in Fig. 2. One sees from the linear regression lines that the London field dependence is followed over a wide range of fields and temperatures. Deviations from linearity occur at low fields.
when $H$ approaches $H_{c1}$ where simple London theory is not valid, and at low temperatures where the materials are sufficiently hysteretic that the averaging procedure illustrated in Fig. 1 is not valid. From Eq. 4 the slopes of the curves in Fig. 2 we obtain values for the London penetration depth $\lambda_{ab}(T)$ in the virgin material. These results will be compared and contrasted with values deduced for the irradiated Hg-1223. In addition, the intercepts provide a measure of the upper critical field $e^{1/2}\beta_{c2}(T)$, where $e \approx 2.718...$ is the natural logarithm base. We now compare these results with those from a scaling analysis.

Recently, Landau and Ott demonstrated a useful scaling methodology based on Ginzburg-Landau theory. This has been applied to both single crystal and aligned particle arrays and more recently to randomly oriented, polycrystalline superconductors. If one assumes that the Ginzburg-Landau parameter $\kappa = \lambda/\xi$ is independent of temperature, then $M_{eq}(H,T)$ is a unique function of $H/H_{c2}(T)$. Consequently it follows that the equilibrium magnetizations in field $H$ at temperature $T$ and (arbitrary) reference temperature $T_0$ are related as follows:

$$M(H,T_0) = M(h_{c2}H/T)/h_{c2} \quad (4)$$

where $h_{c2} = H_{c2}(T)/H_{c2}(T_0)$. To apply this scaling relationship, we chose $T_0 = 85$ K and manually varied $h_{c2}$ to superposition the data for each temperature. (While a term of the form $c_0(T)H$ was included in the original analysis to account for additional contributions to $M$, we took a minimalist approach of having $h_{c2}$ as the sole parameter.) The results are shown in Fig. 2 which plots $M/h_{c2}$ versus $H/h_{c2}$ for a wide range of temperatures. Given the simplicity of the approach, the scaling is quite good. The results for $h_{c2}(T)$, shown in the lower inset, are well behaved. Following Landau and Ott, we fit the temperature dependence to an expression of the form

$$h_{c2}(T) = h_{c2}(0)[1-(T/T_c)^\mu] \quad (5)$$

for $T \geq 90$ K. This describes the data well (solid curve in the lower inset) and yields $\mu = 2.5$ and $T_c = 134$ K, which is quite close to the diamagnetic onset of 133 K measured in low field. Unfortunately, the scaling analysis provides only relative values for $H_{c2}$. So it is useful to compare these results with the corresponding determinations of $\beta H_{c2}$ from the London analysis. This comparison is shown in the upper inset to Fig. 2. The error bars show one standard deviation and the straight line illustrates a simple direct proportionality. While there seems to be a systematic deviation from such a simple relation, most data lie within two standard deviations of a linear dependence.

![Fig. 1: (color online) The magnetization of virgin Hg-1223 at 80 K, versus applied magnetic field (log scale). Open squares show the measured $M$ in increasing and decreasing field history, while closed squares show the average $M \approx M_{eq}$. The solid line is a fit to the conventional London $\ln(H)$ dependence. Data for Hg-1223 containing randomly oriented columnar defects are included for comparison.](image1)

![Fig. 2: (color online) The equilibrium magnetization $M_{eq}(H,T)$ plotted vs $\ln(H)$ for unirradiated Hg-1223 at the temperatures shown. Lines are fits to conventional London theory.](image2)

**B. Equilibrium Properties of Hg-1223 with Randomly Oriented CDs**

We now address the question of how the addition of randomly oriented columnar defects modifies the equilibrium magnetization in the mixed state. The qualitative effects of the CD’s are illustrated in Fig. 1 which includes data for $M_{eq}$ at 77 K for irradiated samples with...
defect densities $B_\Phi \approx 1.0$ and 3.4 T. Comparing these data with the virgin curve shows that the CD’s reduce considerably the magnitude of the equilibrium magnetization, especially at lower fields. In addition, they generate a pronounced deviation from the “standard” London field dependence, giving $M_{eq}$ an “$S$”-like dependence on field. This “anomalous” behavior has been observed previously in cuprates containing parallel columnar defects formed by 5.8 GeV Pb-ions, in thallium-based single crystals\textsuperscript{19} in Bi-2223 tapes\textsuperscript{20}; and in Bi-2212 single crystals\textsuperscript{19,20}.

These changes in the equilibrium magnetization have been attributed to magnetic interactions between the vortex lattice and the columnar defects. By occupying a pinning site, a vortex gains pinning energy. This reduction in system energy must exceed the energy increase arising from direct intervortex repulsion when a vortex is displaced from its natural position in the lattice to a particular columnar defect. For a defect geometry with parallel tracks that have a Poisson distribution of separations, Wahl et al.\textsuperscript{13} obtained an expression for $M_{eq}$ that describes reasonably well the “$S$”-shaped field dependence in Ti-cuprate crystals containing parallel CD’s.

In the Hg-cuprates investigated here, one might expect that the randomly oriented columnar microstructure should entangle the vortices. Consequently it is somewhat curious that the $M_{eq}$ in polycrystalline materials with random CD’s can resemble single crystals with parallel defects. The operative ‘refocussing’ process is sketched in Fig. 4 (a). In real space, the sample consists of grains randomly oriented with respect to the applied field $H$. (b) After irradiation, there are CD’s randomly oriented about the $c$-axis, which makes some angle $\theta_H$ with respect to an applied magnetic field. Now, for highly anisotropic single crystals, it is long recognized that only the normal component of field is effective.\textsuperscript{17} More generally, rescaling gives a field $	ilde{H}$ lying near the $c$-axis; similar arguments\textsuperscript{10} lead to a “refocussing” of the CD’s into a narrow distribution about the $c$-axis. According to the theoretical development,\textsuperscript{10} the complexity of randomly oriented columnar defects in a polycrystalline material is reduced to a considerable degree by a large superconducting anisotropy, restoring the simple physics of a crystal with parallel pins. Indeed, studies of polycrystalline Hg-cuprates demonstrated a recovery of vortex variable range hopping (VRH), very similar to that observed in YBaCuO single crystals containing parallel CD’s.\textsuperscript{21} Among the Hg-cuprates with 1, 2, and 3 adjacent Cu-O layers, the recovery of VRH was most pronounced in the Hg-1223 material with the largest mass anisotropy parameter $\gamma$. We have suggested\textsuperscript{22} that this scenario—an anisotropy-induced “refocussing” of the defects and field toward the crystalline $c$-axis—can account for the “$S$”-like dependence of $M_{eq}$ on field in highly anisotropic Tl-2212 materials, where $\gamma \approx 200$. Here we test and confirm the validity of the rescaling formalism in these Hg-1223 materials with significantly lower $\gamma \sim 60$. Below we show that vortex pinning by random CD’s provides a reasonable qualitative explanation for the reduction in equilibrium magnetization, despite the complexity of the materials in real space.

Let us now use the vortex-defect interaction theory of Wahl et al.\textsuperscript{13} to model our experimental data. From the
theory, one has for $H \parallel c$-axis that

$$M_{eq} = -\left(\varepsilon_0/2\Phi_0\right) \times \ln(\beta H_{c2}/B)$$

$$+ \frac{U_0}{\Phi_0} \left\{ 1 - \left[ 1 + \frac{U_0 B_\Phi}{\varepsilon_0 B} \right] \exp \left( -\frac{U_0 B_\Phi}{\varepsilon_0 B} \right) \right\} \quad (6)$$

where $\varepsilon_0 = (\Phi_0/4\pi \lambda_{ab})^2$ is the line energy, $U_0 \propto \varepsilon_0$ is the pinning energy, and $B = (H + 4\pi M) = H$ since $M$ is small. The first term is the conventional London expression. The second is an added term to account for interactions; it is most significant in intermediate fields and it vanishes in large fields $B \gg B_\Phi$, where vortices greatly outnumber defects. For $H$ inclined at angle $\theta$ from the $c$-axis, one can introduce the angular dependence of the line energy, pinning energy, and $B_{c2}$ via the anisotropy function Eq. (2). An angular average for a randomly oriented polycrystalline material leads to the following:

$$\langle M_{eq} \rangle = -\left(\varepsilon_0/2\Phi_0\right) \times \left[ (1/2) \ln(\beta H_{c2}/B) + (1/4) \right]$$

$$+ \frac{U_0}{2\Phi_0} \left\{ 1 - \left[ 1 + \frac{U_0 B_\Phi}{\varepsilon_0 B} \right] \exp \left( -\frac{U_0 B_\Phi}{\varepsilon_0 B} \right) \right\} \quad (7)$$

Here the symbols have the same meaning as above and we assume that $\gamma \gg 1$.

In using this expression, Eq. 7, to model the data at various temperatures $T$ (77, 90, 100, and 110 K), our objective was to maintain an internally consistent set of parameters. The results are shown as solid lines in Fig. 5a for the sample with $B_\Phi \sim 1$ T and in Fig. 5b for the sample with a higher defect density. Given the complexity of the polycrystalline material and of the vortex and defect arrays, the description of the experimental data (filled symbols) is relatively good. The results of the pinning energy are a significant fraction of the line energy and are quite reasonable, with $U_0 = 0.8\varepsilon_0$ for both materials. To obtain reasonable modeling of the data for the two irradiated materials, we used values of 1.4 and 2.8 T, respectively, for the effective defect densities $B_\Phi$. The differences from the nominal values (calculated from the proton fluences) may arise from some overlap of tracks at the highest fluence combined with uncertainty in calculating the production rate for CD’s. In analyzing the more highly anisotropic Tl-2212 materials ($\gamma \approx 200$), comparable modeling was achieved with $B_\Phi$ values varying by $\sim 20\%$ from those calculated from the proton fluence.

An important feature of any superconducting material is its London penetration depth. Figure 6 summarizes the results for these materials in a plot of $1/\lambda_{ab}^2$ versus temperature. Values for the virgin sample were obtained from a standard London analysis of the data in Fig. 2. An extrapolation of a Ginzburg-Landau linear dependence near $T_c$ (dashed line) to $T = 0$ yields a value $\lambda_{ab}(T = 0) = 174$ nm, but the implied $T_c$-value is too high. Alternatively, we can invoke the underlying assumption of the scaling procedure that $\kappa$ is temperature independent, which means that $1/\lambda_{ab}^2$ should have the same temperature dependence as $h_{c2}$. Hence we fit the present data for the virgin sample ($T \geq 90$ K) with the same temperature dependence in Eq. 8 using the same values for $T_c$ and $\mu$ and varying only the prefactor $1/\lambda_{ab}^2(T = 0)$, obtaining $\lambda_{ab}(T = 0) = 157$ nm, which is comparable with earlier determinations. The resulting fit (solid line in main figure) is ‘natural,’ as illustrated by the fact that its extrapolation to lower $T$ lies very near the lower temperature data.

In Fig. 6 the $\lambda_{ab}$-values for the materials with CD’s were obtained from the modeling procedure. All of these results are reasonably behaved, with $1/\lambda_{ab}^2$ varying roughly linearly with $T$ at high temperature, but extrapolating to $T_c$-values that are rather high. Thus we also fit the data for the irradiated samples with the temperature dependence in Eq. 8, again setting $\mu = 2.5$ and fixing $T_c$ at the experimental values measured in low field, so that only the prefactor $1/\lambda_{ab}^2(T = 0)$ was varied. The resulting fits, which are shown as solid lines in the main figure, describe the data quite well.

It is clear that proton irradiation increased $\lambda_{ab}$ significantly. This is expected, from two theoretical perspectives. First, conventional GLAG (Ginzburg-Landau-Abrikosov-Gorkov) theory predicts that the penetration depth $\lambda^2$ increases as $(1 + \xi_0/\ell)$ when the electronic mean free path $\ell$ is reduced by scattering, as produced by irradiation-generated defects from neutrons and secondary protons released by spallation. Second, the theory of Wahl-Buzdin provides that introducing CD’s increases the penetration depth as

$$\lambda^{-2}(B_\Phi) = \lambda^{-2}(B_\Phi = 0) \times \left[ 1 - 2\pi R^2 B_\Phi/\Phi_0 \right] \quad (8)$$

where $R$ is the radius of a columnar track. The combi-
FIG. 6: (color online) The temperature dependence of the London penetration depth $1/\lambda_{ab}^2$. Values for the virgin sample come from a conventional London analysis of the data in Fig. 5, for the irradiated materials, values come from modeling the equilibrium magnetization shown in Fig. 6. Inset shows values for $1/\lambda_{ab}^2$, extrapolated to $T = 0$, plotted versus defect density; square symbols denote $B_\Phi$ values calculated from the proton fluence and circular symbols are values used in the modeling.

An interesting consequence of a larger London penetration depth is that the vortex line energy $\varepsilon_0 \sim 1/\lambda_{ab}^2$ decreases significantly. As a result, one can expect the vortex pinning energy of a CD and its pinning force to decrease, reducing its effectiveness. A progressive decrease of $\varepsilon_0$ can be expected to counteract the nominally positive influence of increasing the defect density $B_\Phi$. Consequently it is interesting and useful to examine how the irreversible properties of the materials change with defect density, which we now consider.

C. Irreversible Properties and Persistent Current Density

As is well recognized, the addition of correlated disorder can increase the pinning of vortices, often quite significantly. This is illustrated in Fig. 7, which shows the magnetization $M(H)$ at 60 K vs magnetizing field $H$, for various defect densities. With increasing fluence, the “hysteresis loops” increase in width and become symmetric about the $M = 0$ axis.

For the virgin sample, the asymmetry, in combination with the fact that the decreasing field branch lies near the $M = 0$ axis, suggests that surface barriers contribute to the observed hysteresis in this case. It is interesting to note that a relatively low dosage of CD’s, $B_\Phi = 0.1$ T, symmetrizes the $M(H)$ loop significantly; in particular, the magnitude of $M$ in the decreasing field branch is much larger. These features imply that the addition of CD’s suppresses the surface barrier, as recently discussed by Koshelev and Vinokur.

Using the Bean model, one may obtain the persistent current density $J(H, T)$. For these weakly linked polycrystalline materials, the magnetization reflects the intragranular current density. Some results of this analysis are shown in Fig. 8 and Fig. 9 as plots of $J$ versus temperature $T$, in applied fields of 0.1 and 1 Tesla, respectively. The enhancement in $J$ is modest in low fields; this can be attributed to the presence in the virgin sample of both naturally occurring defects that provide some pinning and the likely influence of surface barrier effects,
as already noted. In higher fields, the contribution of the random CD’s is more apparent and \( J \) is enhanced by about an order-of-magnitude. For high-\( T_c \) materials with these angularly dispersed defects, one generally achieves the maximum \( J \) at some defect density \( B_c \) near 0.2–2 T. This optimization is shown by the insets in Figs. 8 and 9. For an applied field of 0.1 T (Fig. 8 inset), \( J \) at 100 K is largest for \( B_c = 0.1–0.3 \) T. For the second example with a field of 1 T (Fig. 9 inset), \( J \) at 60 K is largest for \( B_c \) near 2 T. Qualitatively, the optimum defect density in each case is comparable with the vortex density, i.e., about \( 2 \times \) larger.

For higher defect densities, the current density \( J \) decreases. This is due primarily to a suppression of the vortex line energy and pinning energy, as a consequence of the large, experimentally observed increases in the London penetration depth. Thus we believe that that the competition between increasing defect density and weakening line energy play a major role in determining the range of \( B_c \) that maximizes the current density \( J \), as illustrated in the insets of Figs. 8 and 9. This competition is reminiscent of the formation of point-like defects in YBa\(_2\)Cu\(_3\)O\(_x\)–\( \delta \), where progressive removal of oxygen creates defects, but also reduces their effectiveness through increases in the superconductive length scales.\(^{30,31}\)

An additional mechanism for reducing \( J \) at higher defect densities may be that the presence of additional CD’s helps to initiate the hopping of vortices to nearby empty pinning sites. A third potential influence is a suppression of \( T_c \); however, the change in \( T_c \) is small and these measurements are far from \( T_c \), so this contribution is expected to be small.

### IV. SUMMARY

We irradiated polycrystalline HgBa\(_2\)Ca\(_2\)Cu\(_3\)O\(_x\) materials with 0.8 GeV protons to produce randomly oriented columnar defects via a fission process. Adding random linear defects significantly reduced the magnitude of the equilibrium magnetization \( M_{eq} \) and changed its dependence on magnetic field from a simple London \( \ln(H) \) form (as observed for the virgin material) to a more complex “S”-shaped dependence. For the virgin superconductor, \( M_{eq}(H,T) \) can be scaled by the relative upper critical field \( h_{c2}(T) \), as recently discussed,\(^{12}\). These results compare reasonably with values from a London analysis. For materials with random CD’s, we invoke an anisotropy-induced “refocusing” of the vortex-defect array and model these results using the theory of Wahl–Buzdin that incorporates vortex-defect interactions. This analysis shows that the addition of random columnar defects increases the London penetration depth markedly. The success of this analysis demonstrates the essential correctness and applicability of the refocussing mechanism in these materials with intermediate anisotropy, \( \gamma \sim 60 \). Enhancements in vortex pinning increased the persistent current density \( J \), with the optimum defect density depending on the range of field and temperature. However, a high density of CD’s increases \( \lambda \) and decreases the line energy, which diminishes their effectiveness for pinning vortices. Finally, the study provides qualitative evidence for the suppression of surface barriers in these Hg-1223 materials by a low density of CD’s. Overall, we find a delicate balance between increases in the density of correlated disorder – randomly oriented columnar defects – and decreases in the equilibrium superconductive
properties, which progressively reduce the effectiveness of each defect added.

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