Searching for Pulsars with Phase Characteristics

Bo Peng1, Qian-Chen Hu1, Qiang Li1, Lei Qian2,3,4,5, Xiao-Bo Dong6, Shi-Lin Peng1, and Ze-Lin Wang1

1 School of Information Engineering, Southwest University of Science and Technology, Mianyang 621010, China; pengball@swust.edu.cn
2 National Astronomical Observatories, Chinese Academy of Sciences, Beijing 100101, China
3 CAS Key Laboratory of FAST, National Astronomical Observatories, Chinese Academy of Sciences, Beijing 100101, China
4 State Key Laboratory of Space Weather, Chinese Academy of Sciences, Beijing 100190, China
5 University of Chinese Academy of Sciences, Beijing 100049, China
6 Yunnan Observatories, Chinese Academy of Sciences, Kunming 650011, China

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Abstract

We present a method by using the phase characteristics of radio observation data for pulsar search and candidate identification. The phase characteristics are relations between the pulsar signal and the phase correction in the frequency-domain, and we regard it as a new search diagnostic characteristic. Based on the phase characteristics, a search method is presented: calculating dispersion measure (DM)—frequency data to select candidate frequencies, and then confirming of candidates by using the broadband characteristics of pulsar signals. Based on this method, we performed a search test on short observation data of M15 and M71, which were observed by Five-hundred-meter Aperture Spherical radio Telescope, and some of the Galactic Plane Pulsar Snapshot survey data. Results show that it can get similar search results to PRESTO (PulsaR Exploration and Search TOolkit) while having a faster processing speed.

Key words: methods: data analysis – (stars:) pulsars: general – stars: neutron

1. Introduction

Pulsars are important in studies of space navigation (e.g., Buist et al. 2011), gravitational wave detection (e.g., Lommen 2015), and interstellar medium (e.g., Manchester & Taylor 1977). For these works, the detection and discovery of new pulsars is meaningful. A typical pulsar search process consists of several steps, i.e., removing radio frequency interferences (RFIs), dedispersion, periodic signal and single pulse searches, and candidate identification. In these processing steps, a large number of intermediate data with different dispersion measures (DMs) will be generated. On the generated data, a further search with different algorithms will be carried out, such as the fast folding algorithm (FFA; Staelin 1969) for long-period signals, acceleration search (Ransom et al. 2000) and phase modulation algorithm (Jouteux et al. 2002) for binary pulsars. With such a large amount of intermediate data and complex search processing, it is a time-consuming process to get those pulsar candidates. As an example, it takes 170 s to process a data set of 26 s observation with a 24 cores computing (Yu et al. 2020). To this end, a bunch of accelerated schemes have been provided, but most of them are carried out under the existing framework, such as using GPU to accelerate on the dedispersion (Barsdell et al. 2012) and acceleration search (e.g., PRESTO7 (PulsaR Exploration and Search TOolkit) on gpu8 by Luo et al. 2022, in preparation), using FPGA as a backend for pulsar dedispersion processing (Luo et al. 2017), or using computer clusters to parallelize the entire search (Yu et al. 2020). These methods have a relatively significant improvement in computing speed, but there are some problems in their application, such as how to deal with the memory computing bottleneck (Sclocco et al. 2016) when using a single machine for dedispersion.

Some new algorithms like Fourier-domain dedispersion (FDD; Bassa et al. 2022), could improve the efficiency of data processing and avoid computational bottlenecks at the same time. However, these new algorithms mainly improve parts of the processing structure rather than the whole search framework. In that way, the overall speed cannot be fully improved when processing the bountiful data emerged in the search. Inspired by FDD, a phase characteristic can be calculated with the discarded phase data after FDD calculation. A DM-frequency image is obtained, showing the influence of DM change on different frequencies. On the basis of FDD, DM-frequency data of the entire data space can be obtained by adding a small amount of calculation, and a method for candidate frequency screening is introduced. With the increase of the observation channels of modern telescopes (Lyon et al. 2016), the phase characteristic can clearly show the situation of the signals in different channels and the broadband and dispersion features of the pulsar signals can also be reflected. According to those features or characteristics, the pulsar candidate signals can be judged and confirmed. Combined

7 http://www.cv.nrao.edu/~ransom/presto/
8 https://github.com/jintaoluo/presto_on_gpu
with FDD, phase characteristic can also be integrated into the traditional search structure, by which broadband characteristic images can be quickly obtained. In order to test, the data of M15, M71 and some of GPPS (Han et al. 2021) data observed by FAST (Nan 2006; Jiang et al. 2019; Jiang et al. 2020; Qian et al. 2020) are used for phase characteristic calculation.

In this paper, we introduce the detailed description of phase characteristic in Section 2. Section 3 presents the search test. The discussion and conclusion are given in Section 4.

2. Methods

2.1. Related Work

A typical time-domain dedispersion algorithm can be described as shifting raw data (a 2D array of fast sampled time series across multiple frequency channels) with dispersion delay based on DM value, and summing up all channels’ data. Equation (1) is the dispersion delay between frequency \( \nu_1 \) and \( \nu_2 \) at a specific DM, based on the Tools of Radio Astronomy (Rohlfs & Wilson 2013).

\[
\frac{d}{d\mu s} = 4.148 \times 10^9 \left[ \frac{\text{DM}}{\text{cm}^{-3}\text{pc}} \right] \left[ \frac{1}{(\nu_1 \text{ MHz})^2} - \frac{1}{(\nu_2 \text{ MHz})^2} \right] \tag{1}
\]

Generally, assuming \( N \) is the number of channels, channel 1 is the standard phase, and \( d_n \) is the dispersion delay under the specific DM between channel 1 and channel \( n \). Then, time-domain dedispersion can be described by Equation (2), in which \( S_c \) is dedispersed data, and \( S_n \) is the raw data of channel \( n \). Obtaining \( S_c \) is a low computational density process, which only requires a few computation time, while most time is used for raw data reading from memory. As the DM is unknown in the process of pulsar search, raw data will be read many times to traverse all possible DMs.

\[
S_c(t) = \sum_{n=1}^{N} S_n(t) - d_n \tag{2}
\]

Based on the time-domain dedispersion algorithm, FDD chooses a different way of data processing. During FDD, Fast Fourier Transform (FFT) is directly performed on the raw data of each channel as Equation (3), in which \( X_n(\omega) \) is the FFT result of \( S_n(t) \), and \( \omega = \{ \omega | \omega = \frac{2\pi i}{T}, i \in [1, \frac{T}{2}] \} \), \( T \) is the number of sampling points. As \( \omega \) is determined by point index \( i \) in frequency domain, we simply use frequency \( \omega_i \) refer to the frequency corresponding to the point with index \( i \). Then, based on the equivalence of frequency-domain phase shift and time-domain shift (Bracewell & Bracewell 1986), rotation factor is used to achieve the effect of dedispersion (see Equation (4)). With the correction of rotation factor \( e^{j\omega_i d_n} \), frequency-domain dedispersed data \( X_c(\omega) \) can be obtained. At the end of FDD, \( X_c(\omega) \) will be turned to time domain dedispersed data \( S_c \) with inverse Fourier transform.

\[
S_{\text{raw}} = \begin{bmatrix} S_1(t) \\ S_2(t) \\ \vdots \\ S_N(t) \end{bmatrix} \xrightarrow{\mathcal{F}} \begin{bmatrix} X_1(\omega) \\ X_2(\omega) \\ \vdots \\ X_N(\omega) \end{bmatrix} \tag{3}
\]

\[
[X_1(\omega) X_2(\omega) \cdots X_N(\omega)] \times \begin{bmatrix} e^{j\omega_1 d_1} \\ \vdots \\ e^{j\omega_N d_N} \end{bmatrix} = X_c(\omega) \xrightarrow{\mathcal{F}^{-1}} S_c(t) \tag{4}
\]

Although the processing results of FDD are still time-domain, the frequency-domain dedispersed data \( X_c(\omega) \) is obtained during the process, which can be directly used in pulsar search, as shown in Figure 1. Compared with the traditional way, FDD has obtained frequency-domain data \( X_n(\omega) \) of each channel, which contains a lot of phase information. However, the phase information of \( X_n(\omega) \) is only used for dedispersion in FDD.

2.2. Phase Alignment

Theoretically, without considering the influence of noise and radio frequency interferences (RFIs), if there is only one pulsar with frequency \( \omega_i \) in the observation data, there will be a peak at frequency \( \omega_i \) in the power spectrum of each observation channel, that is, \( |X_n(\omega_i)| \geq |X_m(\omega_m)|, m \neq i \). However, due to the dispersion, if we directly superimpose these complex vectors like \( \sum_{n=1}^{N} X_n(\omega) \), the peak will no longer be significant. Considering the influence of dispersion as shown in Equation (4), the complex vector sum at frequency \( \omega_i \) is turned to \( X_c(\omega_i) = \sum_{n=1}^{N} X_n(\omega) e^{j\omega_i d_n} \), in which the phase angle of complex vector \( X_c(\omega_i) \) is corrected with \( e^{j\omega_i d_n} \). Note that \( d_n \) is determined by DM, this means in time-domain dedispersion, correct DM aligns the pulses of each channel, while in frequency-domain dedispersion, correct DM aligns complex vectors of each channel at pulsar frequency \( \omega_i \).

That alignment effect can be shown in Figure 2, which is drawn with one of the GPPS data (Ransom et al. 2002 have drawn a similar image to prove the effect of frequency derivative correction). Figure 2 shows that at pulsar frequency 264.2423 Hz, the correct DM aligns complex vectors of each...
channel, making the length of the complex vector sum to be the longest (see the dashed line in Figure 2(a)). However, when using non-pulsar frequency or uncorrected DM, the trajectory of complex vector sum is around the center (see the other line in Figure 2). Compared with the complex vector sum with non-pulsar frequency or uncorrected DM, the complex vector sum at 264.2423 Hz and 25.7 cm$^{-3}$pc has shown remarkable feature of phase alignment, which could be used as a basic component of the pulsar phase characteristics.

2.3. Phase Characteristic for Search

Since Figure 2 contains only a few DMs, Figure 3 is given to show the influence of all possible DMs on the complex vector sum. The red solid line in Figure 3 shows that when the raw data contain a pulsar signal, matching with the correct DM values can maximize the modulus of vector sum at pulsar frequency. However, Figure 3 contains only two frequencies, which is too few compared with the all possible frequencies of raw data.

To show the variation of vector sum with DMs at all possible frequencies, we draw Figure 4, which is called DM-frequency image later. Essentially, DM-frequency image is the visualization of $X_n(\omega_i)$ in Equation (4), while each vertical line in Figure 4 can be drawn as a curve in Figure 3. In addition, the goal of time-domain dedispersion shown in Figure 1 is obtaining a horizontal line of DM-frequency image. Therefore, pulsar phase characteristics presented in this paper can be seen as another perspective of the DM-frequency image.

Since most RFI signals in radio pulsar data are 0 DM signals, the responses of RFIs shown in Figure 4 are lines starting from 0 cm$^{-3}$pc, and the closer they approach to 0, the higher the energy. Excluding RFI signals, candidate frequencies can be filtered to several one ($S_1$, $S_2$) in the center of the image, which is PSR J1905+0400 and its harmonic. Comparing $S_1$ and $S_2$ in the image, which has the same DM, but with a difference in the length of the signal, $S_2$ with higher frequency is much shorter than $S_1$. To make this phenomenon more clear, we draw a simulation image in Figure 5, and simulate phase correction curves for pulsar signals with the same DM but different frequencies.

Figure 5 shows that the simulated signal shows not only a change in peak width as the frequency changes, but also a “sinc like” phenomenon when the signal changes with DM. For the

![Figure 2. Complex vector sum at 264.2423 Hz, 200 Hz and 150.1046 Hz with different DMs. 200 Hz is chosen as the noise frequency, limited by the number of samples, the actual frequency is 199.9982 Hz, which is very close to the terrestrial main utility frequency’s harmonic. 150.1046 Hz is terrestrial main utility frequency’s third harmonic. The outer black circle is $\sum_{i=1}^{N}|X_n(\omega_i)|$, in which $\omega_i$ is 264.2423 Hz in (a), 200 Hz in (b) and 150.1046 Hz in (c), and curves in (a), (b) and (c) show the superposing process of complex vectors of each channel corrected with different DMs. At 264.2423 Hz, the frequency of PSR J1905+0400, correct DM 25.7 cm$^{-3}$pc makes the vector sum align and closest to the outer black circle.](image)

![Figure 3. Use 0–1000 cm$^{-3}$pc as DM with a step size of 1 cm$^{-3}$pc to correct the signals in Figure 2, then superimpose the corrected data of each channel and take the modulus as amplitudes.](image)
change of the width on the peaks, it can be explained from the phase correction equation. With the decrease of frequency $\omega$, $d_n$'s influence on the rotation factor $e^{-j\omega d_n}$ reduces. In other words, under the same DM, the rotation angle of the rotation factor becomes smaller as the candidate frequency decreases, so the higher the signal frequency, the narrower the peak. For a similar reason, the "sinc like" function pattern appears in the curve. For channels close to channel 1, $d_n$ is close to 0, a slight change in rotation factor, different channels have different rotation angles. When the phase changes with DM, some of the channels point in the opposite direction to other channels (as the solid line in Figure 2(a)). The vector sum will appear in the valley area of the curve when these channels account for a large proportion, and it will appear in the peak area with the increase of the similar channels. To those DMs larger than 69.55 cm$^{-3}$pc, the phase angles of different channels become chaotic and the curve becomes flat with the increase of DM value.

Based on DM-frequency image, the search for candidate frequencies can be performed, as such an image can be used to check if a signal with dispersion effects exists. But when it comes to searches in observed data, just relying on DM-frequency image is not enough, just like searches cannot merely rely on pulse profiles for pulsar identification. If strong RFIs or noises exist in some channels, there will still be bright spot in DM-frequency image at the RFI frequency. To distinguish the bright spot brought by RFI and pulsar, we use the broadband characteristic of pulsar signals, that is pulsar signals exist in most channels. To reflect broadband characteristic in frequency domain, we divide channels into groups and perform a group by group accumulation at candidate frequency. Then, the broadband characteristic can be reflected with a 2D image like Figure 6, which we call multi-channel phase alignment.

With the multi-channel phase alignment image, candidate frequencies in DM-frequency image like $S_1$ in Figure 4 can be further judged. The broadband characteristic of $S_1$ has been presented in Figure 6(a), which is almost a straight line throughout the observed frequencies. For the noise like frequency 200 Hz we chosen, broadband characteristic does not appear, which is an effective differentiation. In addition, to those RFI signals with a DM value of 0 (as Figure 2(c)), such image is similar to moving the vertical line to 0 cm$^{-3}$pc in Figure 6(a). To the difference between broadband and narrowband for signals is whether the strongest positions of each channel group are close to form a straight line.

### 2.4. Data Filtering and Search Structure Design

As candidates frequencies can be filtered with DM-frequency image and further judged with multi-channel phase alignment images, the searches can be defined as follows:

#### (a) Multi-channel phase alignment of PSR J1905+0400 ($S_1$)

![Multi-channel phase alignment of PSR J1905+0400 ($S_1$)](image)

#### (b) Multi-channel phase alignment of 200 Hz

![Multi-channel phase alignment of 200 Hz](image)
alignment image, a complete search framework can be built. However, to draw a DM-frequency image like Figure 4, we need traverse all frequencies, just like traversing all DMs in time-domain, which means a huge amount of computation. Noting that Figure 4 only contains a few candidate frequencies with energy anomalies, while most of the data are abandoned in the subsequent calculations, which means phase corrections of those abandoned data are not necessary, and phase corrections can be performed for a few high energy frequencies rather than all frequencies.

To obtain high energy frequencies, through summarizing the experience of data processing, we propose an empirical method. The method calculates the sum of each channel’s power spectrum, which is the radius of the outer black circle in Figure 2, and filters top ranked frequencies. According to the processing results of PMPS (Parkes Multibeam Pulsar Survey) data and other data, the filtering ratio that we recommend is 1%. Obviously, it is impossible that all of the top 1% are candidate frequencies, so further filtering is performed on the top 1% frequencies after phase corrections. As shown in Figure 2, the correct DM and frequency align complex vectors of each channel, and make the complex vector sum closer to the outer black circle than other DMs or frequencies. Therefore, we use the ratio of the length of complex vector sum to the sum of each channel’s power spectrum as a further filter parameter.

After the two-step filtering, we obtain the multi-channel phase alignment images of candidate frequencies and simplified DM-Frequency image for manual confirmation. The whole search processing flow is shown in Figure 7, in which the search structure is compared with the typical search method. Our processing code is already placed on GitHub.

### 3. Results

#### 3.1. Test Data

In this part, a verification of the phase characteristic based searching method is performed with a group of test data, which
contains two globular clusters with short observation time and two GPPS data files. Each GPPS data can survey a cover of a sky area of 0.1575 square degrees and contains 76 adjacent observation points. The observation information of all test data is shown in Table 1. In these test data, several pulsars have been involved, which are listed in Table A1.

3.2. Time Performance

First, we discuss the time performance of our method, and use PRESTO as a comparison. Table 2 shows the processing time cost on different test data. In Table 2, PRESTO search refers to the time spent in dedispersion, FFT and acceleration search, while the dedispersion plan is given in Table A2. With the same dedispersion plan, we performed phase characteristic search with CPU and GPU respectively, and the time consumption shown in Table 2 refers to the time spent in FFT, power spectrum filter, phase correction and candidate signal filter shown in Figure 7. All tests are handled by the same NH55AF laptop, while both PRESTO search and phase characteristic search with CPU in Table 2 are calculated with one thread. Since our method has not done any special processing for binary pulsars, the acceleration search in PRESTO is turned off and the related parameter ZMAX is set to 0. From Table 2, our method shows a speedup of about 4 times than PRESTO with CPU, which can be further accelerated about 8 times with GPU.

3.3. Sensitivity Comparison

After the search with our method, hundreds of possible signals will be obtained, which can be drawn as a simplified DM-Frequency image like Figure 8 for fast manual search. However, in Figure 8(a), M15’s DM-Frequency image contains PSR J2129+1210A (9.03 Hz) and its numerous harmonics. These harmonics even masked other signals, making it hard to distinguish $S_2$ (PSR J2129+1210B, 17.81Hz) from J2129+1210A’s harmonic $S_1$ in the image. To distinguish $S_2$ from $S_1$, we can draw a 3D image like Figure 9, which shows that the harmonic of $S_1$ covers other signal.

Figure 9 can be regarded as the local amplification of Figure 8(a) around $S_2$, but it is not necessary to draw a 3D diagram like Figure 9. In practical use, we suggest using the simplified DM-Frequency image as a tool to quickly determine whether there is any pulsar candidate existing, then separating the possible candidates with the multi-channel phase alignment images manually. Here using M15 as an example, it can be preliminarily confirmed that one or more pulsars exist in M15 from Figure 8(a). Then, we check all the multi-channel phase alignment images generated, eliminate the influence of harmonics and RFI manually, and obtain pulsar candidate signals ($S_1$, $S_2$, $S_3$) with M15 database, which is actually the PSR J2129+1210A, B and D.

According to the search results of PRESTO, the signal-to-noise ratio of PSR J2129+1210D ($S_3$ in Figure 8(a)) is even weaker than the 37th harmonic of PSR J2129+1210A, but it is still remarkable in Figure 10(a). As a comparison, we give PRESTO’s folding result of PSR J2129+1210D in Figure 10(b), in which the sub-bands folding diagram is

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10 https://fast.bao.ac.cn/cms/article/172/
11 CPU:3900X, GPU:RTX2070m, RAM:32G, SSD:PM981 512G.
similar to Figure 10(a). These two diagrams have a great similarity in the expression of broadband characteristics, except that one uses time domain for presentation and the other uses frequency domain, while the contrast of the frequency domain diagram is stronger.

The search results of test methods and the known pulsars are placed in Table 3. Based on the data of the FAST Globular Cluster Pulsar Survey (Pan et al. 2021), there should be 14 pulsars in M15 and M71: PSR J2129+1210A-I, PSR J1953+1846A-E. Given that we used data with a much shorter observation time than them, the number of detectable pulsars in test data should be less than 14. Compared with the PRESTO processing results, the number of pulsars found with the phase characteristic search method is almost consistent with the detectable pulsars in test data.

For the two GPPS test files, after querying and comparing on the ATNF website, two known pulsars can be found: PSR J1848+0604 and PSR J1905+0400 (in Section 2.2). However, the PSR J1906+0352g found by Han et al. (2021) cannot be sought out by our method, while only the harmonic of PSR J1906+0352g can be found. In Figure 11, (a) and (b) correspond to PSR J1848+0604 and PSR J1906+0352g’s 4th harmonic respectively. PSR J1848+0604 has a low frequency, the resolution of the drawn image is not enough to distinguish its frequency. But the higher energy makes it easier to distinguish from the data. To the signal of PSR J1906+0352g, it is much weaker than PSR J1848+0604, due to the influence of noise, only some harmonics can be found. For such missing signal detection, it reminds us of the necessity of harmonic processing for phase characteristics which have a great help for weak signal detection.

4. Discussion and Conclusion

We have presented a method making use of phase characteristics for pulsar search and tested its feasibility by processing the data of M15, M71, and so on. The pulsar signals are searched and confirmed in the light of their characteristics. Such a method can be used to achieve faster search, and the phase characteristic can also be integrated into the traditional search structure with FDD, which only needs to save the intermediate processing data during the FDD processing. In the candidate signal judgment step of the pulsar search, DM-Frequency images can quickly assist researchers to establish the relationship between the frequency of the data and the DM, especially for pulsars with many harmonics. Based on the two-step filtering, only a few frequencies need to be processed to verify the broadband characteristics of the pulsar.
characteristic. Therefore, the processing scale required by our method is much smaller than PRESTO, so the calculation time is also reduced.

For our method, there are still some problems that need to be solved, the known problems are as follows: (1) the screening in the existing search process is carried out with empirical parameters, how to build an accurate mathematical model to complete the screening. In candidate filtering, there may be a more suitable probability model, how to optimize the existing model and add it to the search process could be a problem. In addition, the further processing of harmonics is also needed to add. (2) The phase characteristics still depend on the calculation results of FFT. This means that it is difficult to find those low-frequency signals masked by red noise, which is also faced by other search methods (Van Heerden et al. 2017). (3) Since there is no additional algorithm adjustment for binary pulsars, it is hard to say that the phase characteristic which is obviously suitable for some bright data such PSR J1953 +1846A can also fit for faint binary pulsars data. (4) For some very short orbit period binary pulsars or binary pulsars of long observation time data, they will produce a palpable frequency shift effect when they rotate (Ransom et al. 2003). The pulse phase of the received data after Fourier transform cannot reflect the information of the signal, which also needs to be concerned. However, to our joy, it is at least clear that what kind of data can be processed by our method.

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Appendix
Pulsar Information

Table A1
Pulsar Information Involved in This Paper

| PSR            | $F_0$ (Hz) | DM (cm$^{-3}$pc) | References       | Notes                                      |
|----------------|------------|------------------|------------------|--------------------------------------------|
| J2129+1210A (M15A/B2127+11A) | 9.03       | 67.31            | Anderson (1993)  |                                            |
| J2129+1210B (M15B/B2127+11B)  | 17.81      | 67.69            | Anderson (1993)  |                                            |
| J2129+1210D (M15D/B2127+11D)  | 208.21     | 67.3             | Anderson (1993)  |                                            |
| J1953+1846A (M71A)          | 204.58     | 117              | Hessels et al. (2007) |                                           |
| J1848+0604                 | 0.4507     | 242.7            | Lorimer et al. (2005) |                                           |
| J1905+0400                 | 264.24     | 25.69            | Gonzalez et al. (2011) |                                           |
| J1906+0352g                | 3.50       | 372              | Han et al. (2021) | Pulsar was discovered after the publication of the paper |

Table A2
Details on Dedispersion Plan for Test Data

| DATA            | DM Start (cm$^{-3}$pc) | DM End (cm$^{-3}$pc) | DM Step (cm$^{-3}$pc) | Down Sample | Number of DMs | Notes                                      |
|-----------------|------------------------|----------------------|-----------------------|-------------|---------------|--------------------------------------------|
| M15             | 0.0                    | 1005.0               | 0.3                   | 4           | 3350          | prepsubband function with 256 nsub         |
| M71             | 0.0                    | 1005.0               | 0.3                   | 4           | 3350          | prepsubband function with 256 nsub         |
| GPPS File       | 0.0                    | 1005.0               | 0.3                   | 4           | 3350          | prepsubband function with 256 nsub         |

ORCID iDs

Bo Peng https://orcid.org/0000-0003-0579-3014

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