Breaking the superfluid speed limit in a fermionic condensate

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Coherent condensates appear as emergent phenomena in many systems. They share the characteristic feature of an energy gap separating the lowest excitations from the condensate ground state. This implies that a scattering object, moving through the system with high enough velocity for the excitation spectrum in the scatterer frame to become gapless, can create excitations at no energy cost, initiating the breakdown of the condensate—the well-known Landau velocity. Whereas, for the neutral fermionic superfluid \(^3\)He-B in the \(T = 0\) limit, flow around an oscillating body displays a very clear critical velocity for the onset of dissipation, here we show that for uniform linear motion there is no discontinuity whatsoever in the dissipation as the Landau critical velocity is passed and exceeded. Given the importance of the Landau velocity for our understanding of superfluidity, this result is unexpected, with implications for dissipative effects of moving objects in all coherent condensate systems.

The Landau critical velocity marks the minimum velocity at which an object moving through a condensate can generate excitations with zero energy cost. In the frame of the object, moving at velocity \(\mathbf{v}\) relative to the fluid, excitations of momentum \(\mathbf{p}\) are shifted, by Galilean transformation, from energy \(E\) to \((E - \mathbf{v} \cdot \mathbf{p})\). Superfluid \(^3\)He-B has a BCS dispersion curve with energy minima, \(E = \Delta\) at momenta \(\pm p\). Therefore, excitation generation should begin as soon as one energy minimum reaches zero, that is, when the velocity reaches the Landau critical value, \(v_L \approx \Delta/|p|\).

We can investigate \(v_L\) in condensates in two limiting regimes, that is, for the motion of microscopic objects (for example, ions) or for that of macroscopic objects. For ions, the critical velocity has been observed in superfluid \(^4\)He at the expected value of approximately \(46\) m s\(^{-1}\) at 25 bar (ref. 10) (at lower pressures vortex nucleation sets in at lower velocities and the critical velocity is difficult to measure), and confirmed in superfluid \(^3\)He-B at 18 bar as being consistent with the expected \(67\) mm s\(^{-1}\) value. For macroscopic objects, the onset of extra dissipation at \(v_L\) in superfluid \(^4\)He cannot be observed since damping from vorticity becomes prohibitive at much lower velocities. However, while macroscopic objects can be readily accelerated at the lowest temperatures to the much lower critical velocities in superfluid \(^3\)He, the experimental picture is not so straightforward.

In superfluid \(^3\)He, oscillating macroscopic objects do indeed show a sudden increase in damping, but at a velocity of only \(\approx v_L/3\), arising from the emission of quasiparticle excitations from the pumping of surface excitations driven by the reciprocating motion. Although this mechanism does not involve bulk pair-breaking, it has created the impression that a Landau critical velocity has indeed been confirmed in \(^3\)He, which is not the case.

What should we expect for uniform motion? The textbook prediction suggests that at \(v_L\), all details of the process become irrelevant.

Figure 1 | The experimental cell. a, View of the nested demagnetization cooling cell (outer cell muted). The adiabatic demagnetization refrigerant comprises high-purity copper plates coated in sintered silver for thermal contact and immersed in the superfluid \(^3\)He sample filling the cell that is cooled to \(140\) \(\mu\)K. b, The moving-wire 'goalpost' (crossbar width 9 mm) is driven perpendicular to its plane through the \(^3\)He and can move over a horizontal distance of \(\pm 6\) mm before touching the inner cell wall. Its position is sensed by detection coils in the outer cell. The temperature, or thermal quasiparticle density, is monitored by vibrating wire and quartz tuning fork resonators. We calibrate the position of the wire by moving it until it is stopped by the cell wall in each direction (see Methods) providing the two fixed points needed to determine the absolute position. The temperature rise caused by the dissipation is monitored by the vibrating wire and quartz tuning fork thermometers.

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Figure 2 | The sustained d.c. velocity method and measurement. The upper panel shows the very accurate linear stroke of the moving wire, sustained over a distance of 2 mm, with blue bands indicating the periods of initial acceleration and of final deceleration. The lower panel shows the associated temperature response, with the period of the linear motion shown by the red band. The line shape is consistent with a burst of dissipation during the initial acceleration and a second during the final deceleration (see Methods). (In principle, we could infer the drag force from the feedback current needed to maintain the uniform motion of the wire. Unfortunately, the wire inertia dominates, and any contribution from the liquid is negligible.)

Condensate breakdown becomes inevitable; the constituent Cooper pairs separate; and the properties rapidly approach those of the normal liquid. Under our experimental conditions, this should be spectacular, since the damping force in the normal fluid is some five orders of magnitude higher than that of the superfluid. Despite this expectation that at \( v_L \) the dissipation should suddenly increase to very high values, here we show that in fact no discontinuity at all is observed in the damping as \( v_L \) is exceeded.

The measurements are made in \(^3\)He at zero pressure, between 140 and 190 \( \mu \)K (in the quasiparticle ballistic limit) in the cooling cell shown in Fig. 1 (see Methods). The macroscopic ‘moving object’ is a wire formed into a rectangular shape. We can move the wire over a range of velocities in two ways: with a single stroke of steady uniform velocity; or by oscillation at 66 Hz, the mechanical resonant frequency. For oscillatory motion the damping force as a function of velocity is directly measured from the resonance. For steady motion we infer the damping from the thermal response, as shown in Fig. 2. Since the temperature profile of rise and slow return to equilibrium is invariant in our temperature range, we derive the damping force from the pulse height as explained in Methods. We should emphasize that the damping comes almost entirely from the emission of quasiparticles with only a microscopic fraction going into vortex creation.

Figure 3 shows the velocity dependence of the damping force on the moving wire for both a.c. and d.c. motion at around 150 \( \mu \)K. The oscillatory motion shows the expected rapid rise starting at approximately \( v_L / 3 \). However, the d.c. results are strikingly different, showing only a very slow rise, again starting at \( \approx v_L / 3 \), but with no discontinuity whatsoever on passing either \( v_L / 3 \) or \( v_L \).

A hint to the processes involved comes from the oscillatory behaviour, for which we have a reasonable understanding. We use a simple model where we assume a gas of quasiparticle states in the region of depressed gap near the wire surface. The precise nature of these states is complex since the order parameter near the wall has directional structure depending on the scattering nature of the surface. The states may have Majorana and Andreev bound-state properties. However, in the plane of the surface we assume these states are mobile and have a gapless dispersion curve. This provides a toy model for presenting the data but cannot be far from the truth as these states must transform seamlessly into bulk quasiparticle states as the energy exceeds the bulk gap. The states that dominate the process are those at the extrema of the wire surface where the superfluid backflow is greatest. Figure 4 shows the appropriate dispersion curves in the plane of the wall and along the direction of...
At wire surface

Bulk liquid

Cross-branch process

Escape process

v = 0

v = Δ/3p_F

v < Δ/3p_F

(a) At wire surface
(b) Bulk liquid
(c) Cross-branch process
(d) Escape process

Figure 4 | The processes involved in oscillatory (a.c.) motion. Shown are the dispersion curves for the assumed zero-gap excitations at the cylindrical wire surface (in black) and those fully gapped in the bulk liquid (blue) (see text). We use the convention of showing all of the filled states at T = 0 (red, quasiparticles; blue, quasiholes). For pure potential flow the maximum fluid velocity is 2v when the wire moves at v. a. Wire at rest. b. Wire moves slowly; surface-state curves tip by 2v_p and bulk by v_p; surface-state excitations scatter elastically (‘cross-branch’). c. Excitations start to enter the bulk when v = Δ/3p_F (‘escape’); dissipation begins. d. Quasiparticle distributions reach equilibrium with moving wire; escape processes cease. For clarity, only the panels in a have labelled axes.

motion of the wire, for both surface and bulk states, in the moving-wire frame. For simplicity, we assume that T = 0 and that the surface states have zero gap. (Note that owing to the pure potential flow field around a cylinder, when the wire moves at velocity v, the liquid at the wire surface moves at a maximum relative velocity of 2v.)

As the wire moves, the surface-state dispersion curve tips. Elastic collisions with the wire allow excitations to cross the curve (the cross-branch processes of Fig. 4b), populating states on the right-hand side (RHS) and depleting those on the left-hand side (LHS). Given a constant velocity, at some point the distribution of excitations comes into equilibrium with the wire (Fig. 4d). However, if we accelerate the wire fast enough to prevent these cross-branch processes from maintaining equilibrium, excitations on the LHS can now escape directly into the LHS minimum of the bulk dispersion curve. However, again nothing sudden occurs at this point, only steady growth in the escape probability.

We can draw two conclusions. First, this can happen only if the cross-branch processes are relatively slow, but not too slow. If very fast, the branch distributions would always remain in equilibrium with the wire (as in Fig. 4d where no escape process is possible at \( v = \Delta/3p_F \)), and if very slow, no branch equalization occurs at all and again no escape processes are possible.

Second, this must be a transient effect, since at constant velocity the cross-branch processes must ultimately prevail and the distribution will become that of Fig. 4d. In other words, as we accelerate the wire we should see a pulse of excitations emitted as soon as the velocity reaches \( v = \Delta/3p_F \), but if the velocity increases no further, the number of excitations able to escape will become depleted and the dissipation will cease. Of course, in oscillatory motion this does not happen since on reaching maximum velocity, the motion reverses and the whole process repeats in the opposite direction, with the emission of further excitations.

Now consider the effect of an initial acceleration to a sustained steady velocity. Starting from zero we will see the same behaviour as in Fig. 4a–c. As the velocity increases beyond \( v_1/3 \), surface states over a larger region around the wire can access the escape process (that is, not just at the points of maximum surface flow velocity), as in Fig. 5. This increases both the escape probability and the angular range of emission\(^1\), increasing the damping force during acceleration (Fig. 5a,b). When \( v_1 \) is reached (Fig. 5c), a new escape process does indeed become available as quasiparticle excitations on the LHS can now escape directly into the LHS minimum of the bulk dispersion curve. However, again nothing sudden occurs at this point, only steady growth in the escape probability.

Suppose the acceleration stops to give a final steady velocity above \( v_1 \). The surface excitation distributions will gradually come into equilibrium with the wire, cutting off the escape processes. Thus, in this steady state the dissipation ceases. Subsequently, during the deceleration at the end of the stroke, the converse process comes into play yielding a further burst of escaping excitations.

For finite temperatures, we already know the damping force arising from the background of thermally excited quasiparticles\(^1\) (blue dashed line in Fig. 3). The escape processes add the extra component indicated in Fig. 3, but there is no jump at \( v_1 \).

We emphasize that these are mechanisms for promoting local surface excitations into the bulk condensate. (This is rather akin to the ‘baryogenesis’ analogue seen when excitations localized in vortex cores are ejected when the vortices are moved\(^19\)) Paradoxically, there is no mechanism for breaking of Cooper pairs in the bulk, despite the wire moving through the condensate at a velocity above the pair-breaking minimum.

Of course, the Landau argument has to be correct, but it seems that for ‘He-B, the ‘boundary layer’ of depressed gas shields the bulk superfluid from the ravages of the Landau process. This ‘shielding’ arises because, at near-zero temperature, there is no mechanism for the condensate to gain information about what the moving body is.
cross-branch process
\[ v > \Delta/p_F \]

escape process
\[ v \rightarrow \Delta/p_F \]

\[ v = \Delta/3p_F \]

\[ v = \Delta/p_F \]

\[ v \rightarrow \Delta/p_F \]

doing on the other side of the boundary layer. Related effects are seen in rotating superfluid \(^3\)He-B where at very low temperatures the lack of normal fluid disconnects the superfluid from the rotating container\(^{19-21}\). Conversely, microscopic objects (smaller than the coherence length) in the liquid have only a marginal disturbing effect on the superfluid order parameter and are thus fully exposed to the bulk condensate.

Our results were consistent up to 190 \(\mu\)K. At higher temperatures, the growing normal fluid fraction must come into play to transmit this information to the bulk condensate, allowing the ‘classical’ critical velocity behaviour to emerge. Unfortunately, the greater dissipation from the increasing normal fluid fraction rules out measurements in this regime. Perhaps this effect can be studied only in our ‘pure’ condensate. For the future, the same process could be profitably studied in \(^3\)He-A where, depending on orientation, the anisotropic order parameter presents either a full BCS gap or nodes where \(v_c\) would be zero\(^{22,23}\).

The results reported here should be of relevance to other fermionic condensates as well as to superfluid \(^3\)He. Further, the lack of any great increase in the damping force as an object moves through the superfluid above the Landau velocity suggests that it may be possible to construct mechanical devices immersed in the superfluid. For example, small pumps with minimal dissipation would have many uses.

**Methods**

Methods, including statements of data availability and any associated accession codes and references, are available in the online version of this paper.

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Author contributions
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Competing financial interests
The authors declare no competing financial interests.
Methods

The experiments are made in a Lancaster-style nested nuclear demagnetization cell\(^3\) for cooling liquid \(^{3}He\) (see Fig. 1). The moving wire is mounted inside the lower end of the inner cell. Its position is determined by two detector coils in the outer cell. The wire is a 100 \(\mu\)m diameter superconducting NbTi wire bent into a goalpost shape as shown, with height 25 mm and leg spacing 9 mm. In the small vertical external field of 73 mT, the Lorentz force on a current passed along the wire generates a transverse horizontal force, allowing us to move the wire or to oscillate it. The experiments are all made in \(^{3}He\)-B at 0 bar pressure, in the temperature range of 140 to 190 \(\text{mK}\). This is in the ballistic quasiparticle limit, where the mean free path of excitations is much larger than any of the dimensions of the experimental cell.

For the a.c. oscillatory mode measurement we use standard techniques\(^2,25\) to measure the moving wire at its resonant frequency, 66 Hz. The a.c. driving current amplitude \(I\) is stepped upwards in small steps. The voltage generated across the resonator, as the crossbar cuts the applied magnetic flux, is determined by a lock-in amplifier at each step. At low velocity, where the wire is very lightly damped, the amplitude sweep must be carried out slowly to avoid unwanted ringing. The current is converted to driving force through the relationship \(F = BdI\), where \(B\) is the magnetic field and \(d\) is the length of the wire crossbar. The measured a.c. voltage \(V\) is converted to velocity using \(v = V/(BD)\).

For the d.c. measurements at steady velocity, the position of the wire is inferred from the response of the pick-up coils to a small high-frequency (92 kHz) signal added to the driving current. To calibrate the wire position, we gradually increase the drive current until the wire touches the cell wall, at which point the signal in the pick-up coil increases no further, a clear signature that the wall has been reached. We then repeat the process in the opposite direction. Knowing the two extreme positions, we can now accurately determine the position of the wire crossbar at any intermediate point, and we can thereby also derive the spring constant of the wire.

To make a measurement, we move the wire at a constant velocity from a starting point to an end point a few millimetres away. The ramp provides a short acceleration period, followed by a period of constant velocity, ending with a short deceleration stage, as shown in Fig. 2. Accelerating and maintaining the constant velocity requires a carefully profiled current ramp, computed from the dynamical properties of the wire-fluid system. This active control removes transient effects at the beginning and end of the ramp to ensure that the wire never moves faster than the target d.c. velocity. This system was developed specifically for these measurements, similar to a scheme devised for driving uniform motion of a comparable oscillator\(^2\). Following each such stroke, the current is slowly ramped back to the starting point and paused for a few minutes to allow the cell to return to thermal equilibrium before the next measurement. We log the output data from the driving current, and that from the high-frequency lock-in amplifier monitoring the rapid changes of the wire position.

The quantity we wish to measure is the dissipation generated by the linear motion. This we track from the resonant response of a nearby 4.5 \(\mu\)m NbTi filament vibrating wire resonator. This acts as a ‘thermometer’ (or quasiparticle density detector)\(^26\) in the superfluid, providing the quantitative measure of the thermal disturbance caused by each stroke. We can also use the quartz tuning fork\(^26\), shown in Fig. 1, with similar results.

From the thermal dissipation produced we can infer the effective damping force on the wire for each stroke. This conversion requires one calibration constant, determined by comparison with the damping force for the oscillatory motion (which is measured directly) at the same temperature. We know the quasiparticle damping very accurately at low velocities \((v \ll v_L)\)\(^29\) and thus we scale the damping force to agree with that measured for the oscillatory motion at low velocities (say, as for the a.c. sweep and d.c. stroke data from Fig. 3 taken at similar temperatures).

Although we see what appears to be only a single thermal transient, our picture of the process implies that we should see an initial burst of dissipation during acceleration and a second burst during deceleration. Unfortunately the thermometer time–constant time is just too long to resolve such a double pulse shape. However, we have confirmed that the overall shape of the measured pulse is consistent with a convolution of two similar-shaped pulses at the beginning and end of the stroke.

Data availability. All data created during this research are openly available from the Lancaster University data archive\(^30\).

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