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Cavity Attenuators for Superconducting Qubits

Z. Wang,1, * S. Shankar,1 Z. K. Minev,1 P. Campagne-Ibarcq,1 A. Narla,1 and M. H. Devoret1,†
1Department of Applied Physics, Yale University, New Haven, CT 06520, USA

Dephasing induced by residual thermal photons in the readout resonator is a leading factor limiting the coherence times of qubits in the circuit QED architecture. This residual thermal population, of the order of $10^{-1}–10^{-3}$, is suspected to arise from noise impinging on the resonator from its input and output ports. To address this problem, we designed and tested a new type of band-pass microwave attenuator that consists of a dissipative cavity well thermalized to the mixing chamber stage of a dilution refrigerator. By adding such a cavity attenuator inline with a 3D superconducting cavity housing a transmon qubit, we have reproducibly measured increased qubit coherence times. At base temperature, through Hahn echo experiment, we measured $T_{2e}/2T_1 = 1.0 (+0.0/−0.1)$ for two qubits over multiple cooldowns. Through noise-induced dephasing measurement, we obtained an upper bound $2 \times 10^{-4}$ on the residual photon population in the fundamental mode of the readout cavity, which to our knowledge is the lowest value reported so far. These results validate an effective method for protecting qubits against photon noise, which can be developed into a standard technology for quantum circuit experiments.

I. INTRODUCTION

The past two decades have witnessed an exponential increase in the coherence times of superconducting qubits [1]. Major breakthroughs include biasing a charge qubit at the charge-noise-insensitive point [2], shunting the Josephson junction with a capacitance to suppress noise in charge [3–5] and flux qubits [6, 7], and shunting the junction with a superinductance to eliminate offset charge noise in a fluxonium qubit [8]. Moreover, in the circuit QED architecture [9, 10], it has been well understood that the readout cavity modifies the electromagnetic environment of the qubit and can thus affect qubit coherence [11, 12]. In recent years, for transmon qubits embedded in 3D microwave cavities [13], energy relaxation times $T_1 > 100 \mu s$ have been frequently observed [14–17]. However, in these experiments, transmon coherence times $T_2$ are much shorter than $2T_1$, indicating qubit coherence is predominantly limited by pure dephasing. An outstanding question in this field is whether $T_2 \approx 2T_1$ can be reproducibly obtained in long-lifetime superconducting qubits.

One of the main dephasing channels that limit $T_2$ is the residual thermal photon population in the readout cavity [18–24]. In the dispersive coupling regime, due to the AC Stark effect, fluctuations in the thermal photon number of the cavity cause random shifts of the qubit transition frequency and thus contribute to qubit dephasing [25]. In the limit of average thermal photon number $\bar{n}_{th} \ll 1$, the induced dephasing rate is proportional to $\bar{n}_{th}$ [20]:

$$\Gamma_{\phi}^{th} = \frac{\bar{n}_{th} \kappa \chi^2}{\kappa^2 + \chi^2},$$

where $\kappa$ is the cavity linewidth, and $\chi$ is the dispersive shift of the qubit frequency per cavity photon. Theoretically, for a 7.5 GHz cavity mode at 20 mK, $\bar{n}_{th}$ is expected to be on the order of $10^{-8}$. However, the $\bar{n}_{th}$’s estimated from measurements of $\Gamma_{\phi}^{th}$ in recent experiments range from $6 \times 10^{-4}$ to 0.15, corresponding to effective mode temperatures between 55 mK and 140 mK [22–24, 26–28]. Understanding the origin of excess thermal photons and reducing $\bar{n}_{th}$ are therefore crucial to enhancing the qubit coherence times and reliably achieving $T_2 \approx 2T_1$.

One source of the excess $\bar{n}_{th}$ is the coupling of the cavity mode to the input and output ports. This coupling opens a channel for auxiliary components in the microwave wiring to affect the temperature of the cavity mode. Examples of such components are commercial cryogenic attenuators, filters, isolators, etc. These components and the teflon insulator in the coaxial cables are difficult to thermalize to the mixing chamber stage of the dilution fridge. Attenuators are particularly important in this regard since they are the dominant dissipation sources in the wiring of a cryostat and ideally form the bath that thermalizes the readout cavity modes. Insulators inside commercial cryogenic attenuators have poor thermal conductivities at low temperatures as do their stainless steel packages. Lately, thermal anchoring of attenuators has been improved by replacing these materials with better thermal conductors and redesigning the circuit layout [23]. Nevertheless, a fundamental restriction in performance arises from the lumped element thin-film resistive network that these attenuators are made of.

An explanation of this challenge and its solution are shown in Fig. 1. In a lumped element resistor, the electric and heat currents are parallel to each other [see Fig. 1(a)]. Given a certain electrical resistance, the order of magnitude of its thermal resistance due to electronic degrees of freedom is subject to the constraint imposed by the Wiedemann–Franz law [29]. For instance, a 50 Ω resistor at 20 mK should have an electronic thermal resistance on the order of $10^8$ mK/µW. Therefore, microwave attenuators at low temperatures are primarily thermalized through electron–phonon interaction and phonon transport [30, 31]. However, this phonon mechanism suffers from a bottleneck since very few phonons are present.

* zhixin.wang@yale.edu
† michel.devoret@yale.edu
Numerical simulations show that under microwatt input power, the temperature difference inside the resistive network of the attenuator can easily reach 100 mK [23]. While it may be reduced by proper choice of materials and circuit layout, thermalizing all materials to 20 mK may be fundamentally impossible, since some thermal gradient is necessary to produce a sufficient phonon heat current.

To overcome this fundamental challenge, we would prefer to use electrons in a Fermi degenerate system to conduct heat, since electronic excitations are always present at low temperatures. We thus consider an alternative dissipation source for microwave radiation—the normal metal walls of a waveguide section. As shown in Fig. 1(b), in a dissipative waveguide, electric current mainly flows within the skin depth of the wall, while heat is conducted by electrons into the bulk metal, perpendicular to the electric current. In principle, such a distributed structure, if made of a good thermal conductor, can realize an improved cold black body radiation environment at microwave frequencies, which is the goal of our work.

We present in this paper a new type of narrowband microwave attenuator based on a cavity realized by a section of dissipative waveguide, which aims at reducing the residual thermal photon population in circuit QED systems. The normal metal cavity is seamless and machined by conventional techniques without any material growth or microfabrication processes. By coupling it to a transmon–cavity system, we measured enhanced coherence times on two qubits in multiple cooldowns, and obtained record-breaking pure dephasing time $T_\phi$ and $\bar{n}_{\text{th}}$ at base temperature, leaving qubit coherence limited by energy relaxation. Because of its simple design and reliable performance, this cold cavity attenuator will provide a useful addition to the state-of-the-art quantum circuit toolbox.

II. CAVITY ATTENUATOR DESIGN

Most commercial cryogenic attenuators have more than 10 GHz bandwidth. However, microwave pulses for qubit control and measurement are centered only around certain frequencies, and thus only narrowband attenuation is required. This forms the basis for the idea of attenuating quantum signals with a dissipative cavity. For instance, to protect a readout cavity at frequency $f_r$ with $\sim 1$ MHz linewidth from excess photon noise, we would like to supplement commercial attenuators with a cavity attenuator. Such a cavity attenuator should: (1) be centered around $f_r$, (2) provide 10–20 dB attenuation on resonance, and (3) have 10–50 MHz bandwidth, which is an order of magnitude broader than the linewidth of the readout cavity (1–5 MHz). In addition, it should be made of a low-temperature-compatible normal metal, such as brass or, even better, oxygen-free high thermal conductivity (OFHC) copper.

Designing a microwave cavity that can be well thermalized to millikelvin temperatures and has a 10–50 MHz internal dissipation rate (internal quality factor $Q_i \sim 500$) is a challenging task, since good thermal conductors also have low electrical conductor loss. Given the resistivity of the material, the quality factor of a 3D cavity resonator is approximately inversely proportional to its surface-to-volume ratio [32]. An order-of-magnitude estimate shows that the smallest dimension of our brass (OFHC copper) dissipative cavity must be in the submillimeter (sub-0.1-mm) regime. Furthermore, the on-resonance power transmission of a two-port resonator is $4\kappa_{1}\kappa_{2}/(\kappa_{1} + \kappa_{1} + \kappa_{2})^2$, where $\kappa_{1}$ and $\kappa_{1,2}$ are the internal dissipation and external coupling rates. 10–20 dB attenuation requires $\kappa_{1} \sim 10\kappa_{1,2}$—the cavity being uncoupled to the couplers.

Fig. 2 shows a physical realization satisfying all these requirements. It is a single-piece brass (260 alloy) block fabricated using wire electrical discharge machining (EDM) [33, 34]. Such a design eliminates seams and therefore their associated loss [35]. Its external dimensions match the commercial WR-102 waveguides. In addition, it can be directly thermalized to the mixing chamber of a dilution refrigerator through copper braids. As sketched in Fig. 2(b), the cavity is rectangular, apart from...
from a cylindrical hole in the middle for initializing wire EDM cutting. Due to the open boundary condition at both coupling ports, the electromagnetic field in the fundamental mode is non-uniform only in the longest dimension that is 22 mm in this device and sets the mode frequency. The 0.3 mm gap sets the internal dissipation rate. We characterized this cavity at room temperature with a calibrated network analyzer. The waveguide couplers on both sides have $\kappa_i \approx \kappa_i/10$. As shown in Fig. 2(d), the transmission peak centers at 7.52 GHz with 14 dB insertion loss. The reflection loss is 2 dB on resonance (not shown). Combined with reflection measurements, we extracted $\kappa_i/2\pi = 54$ MHz.

Based on this design, we fabricated cavity attenuators with different materials and gap sizes. Parameters of three representative devices are listed in Table I. For cryogenic measurements, the temperature of the attenuator block reached 15 mK as verified by $^{60}$Co nuclear orientation thermometry. As seen in Table I, cavity frequencies increase due to thermal contraction at low temperature. Meanwhile, phonon vibrations freeze out, which increases the metal conductivities and reduces the cavity dissipation rates. For brass, a copper-zinc alloy, $\kappa_i$ is reduced by $\sim 20\%$. For OFHC copper, $\kappa_i$ is reduced by around a factor of three, indicating a ten-fold increase in electrical conductivity. Note that this value is smaller than the DC residual-resistivity ratio (RRR) of OFHC copper because of the anomalous skin effect, which appears when the mean free path of the metal is longer than the wavelength of the RF probe signal [36–38]. The dissipation rates of copper cavity attenuators are limited by the smallest diameter of the EDM cutting wires that our machine shop has access to.

| Material   | Brass | Cu   | Cu   |
|------------|-------|------|------|
| Gap (\(\mu\)m) | 300   | 75   | 125  |
| $T = 296$ K | $f_a$ (GHz) | 7.52 | 7.68 | 7.68 |
|            | $\kappa_i/2\pi$ (MHz) | 64   | 69   | 62   |
| $T = 15$ mK | $f_a$ (GHz) | 7.64 | 7.79 | 7.75 |
|            | $\kappa_i/2\pi$ (MHz) | 44   | 19   | 24   |

TABLE I. Resonant frequency $f_a$ and internal dissipation rate $\kappa_i$ of three cavity attenuators measured at room temperature and 15 mK.

III. QUBIT COHERENCE ENHANCEMENT

We tested the performance of these cavity attenuators by coupling them to a circuit QED system and measuring the qubit coherence properties between 13 mK and 120 mK. The experimental setup is shown in Fig. 3. A cavity attenuator is connected to the sole coupling port of the aluminum cavity housing a transmon qubit. Microwave measurement of the cavity can be performed in reflection. This configuration provides maximum protection against incident photon noise—the transmon is not directly exposed to any excess radiation coming from the transmission lines. Consequently, thermal-photon-induced qubit dephasing can be studied in detail. However, this configuration also degrades the measurement signal-to-noise ratio because the readout signal has been attenuated before being amplified by the output chain. This problem could be solved by in situ quantum limited amplification, which is discussed in Sec. V. We note that one of the ideas behind our experiment—introducing a cold dissipation source in the path of quantum signals—is similar to that of a previous work [27]. Alternatively, the qubit dephasing can also be suppressed by reducing the coupling rate of the readout cavity to the output line [21]. Nevertheless, compared to these strategies, our two-cavity modular approach provides more flexibility in experimental design. In addition, the cavity attenuator filters out off-resonance radiation and thus further suppresses the radiative decay of the qubit [11, 12], acting as an effective Purcell filter [39].

The detailed wiring diagram of the dilution refrigerator is shown in Fig. 8. Particularly, we installed 70 dB commercial cryogenic attenuators on the qubit input line, 40 dB of which are mounted to the base stage. We verified that no improvement of qubit coherence times could
be observed by merely increasing the commercial attenuators beyond 40 dB on the base stage (data not shown). We measured the 0.3 mm-gap brass cavity attenuator coupled to a transmon–aluminum readout cavity system. The reflected signal off the combined system, measured using a network analyzer [see Fig. 3(c)], shows two hybridized modes centered at 7.573 GHz and 7.719 GHz. Using the measured trace, we estimated that the mode centered at 7.573 GHz participates 79% in the aluminum cavity and 21% in the brass cavity, while the mode centered at 7.719 GHz participates 21% in the aluminum cavity and 79% in the brass cavity. We used the mode at 7.573 GHz to readout the qubit since it participates more in the aluminum cavity and thus has a larger dispersive shift. The ratio of internal dissipation to external coupling for this readout mode is estimated to be 6:1. Denoting the average photon population of the internal and external baths by $\bar{n}_i$ and $\bar{n}_c$, we have $\bar{n}_i \ll \bar{n}_c$ since the brass cavity is in thermal equilibrium with the mixing chamber. Therefore, we obtain the residual thermal population of the readout mode to be $\bar{n}_{th} \approx \bar{n}_c/7$, indicating 85% of residual photons are dissipated in the cold cavity attenuator.

| Transmon | $f_{pe}$ (GHz) | $\alpha$ (GHz) |
|----------|----------------|----------------|
| A        | 4.75           | 0.25           |
| B        | 5.09           | 0.25           |

TABLE II. $f_{pe}$ and $\alpha = f_{pe} - f_{ej}$ (anharmonicity) of the two transmon qubits in this experiment.

$T_1$ and Hahn echo $T_{2e}$ were measured as a function of temperature for two transmon–cavity systems, labeled A and B, coupled with brass and copper cavity attenuators as well as without an attenuator. As a control experiment, we also measured an aluminum filter with identical dimensions to the copper attenuator that however provides no attenuation on resonance. The transmon frequencies and anharmonicities are listed in Table II. Data taken on transmon A are shown in Figs. 4(a) and 4(b), with experimental conditions summarized in Table III. Each $T_1$ and $T_{2e}$ data point is the average of ten measurements performed over the course of around one hour. From these results we can infer that cavity attenuators dissipate excess photons in the readout mode and suppress photon-induced qubit dephasing. We see in Fig. 4(b) that $T_{2e}$ for transmon A at base temperature is improved by more than a factor of two with cavity attenuators and can exceed 220 µs. Meanwhile, Ramsey $T_{2R}$ (not shown) was also improved from 28–35 µs without a cavity attenuator to 41–43 µs with the brass attenuator and 35–40 µs with the copper attenuator. The difference between $T_{2R}$ and $T_{2e}$ indicates that low-frequency noise in our measurement setup is causing qubit dephasing. However, since the dephasing due to residual thermal photons cannot be filtered out by a single echo pulse [21], we use $T_{2e}$ to inform us about the effect of the cavity attenuator on the residual thermal photon population.

An important figure of merit to quantify qubit dephasing is the dimensionless value $T_{2e}/2T_1 = T_\phi/(T_\phi + 2T_1)$, which is close to its unity upper limit when the dephasing time satisfies $T_\phi \gg T_1$. As shown in Fig. 4(c), at base temperature we measured $T_{2e}/2T_1 = 0.98 (+0.02/−0.08)$ with the brass attenuator. This ratio is 1.00 (+0.00/−0.12) with the copper attenuator. In either experiment, the average $T_\phi$ is close to 10 ms, much longer than $T_1$, indicating qubit coherence is limited by relaxation rather than pure dephasing. If we attribute all the qubit dephasing to the residual thermal photon population in the fundamental mode of the readout cavity, according to Eq. (1), the upper bound of $\bar{n}_{th}$ is estimated to be on the order of $10^{-4}$, corresponding to an effective mode temperature of $T_{\text{eff}} \leq 40–45$ mK. As a comparison, in the absence of cavity attenuators, transmon A in the same measurement setup has $T_\phi \approx 0.3$ ms and $T_{2e}/2T_1 = 0.72 ± 0.12$, indicating $\bar{n}_{th} \lesssim 4 \times 10^{-3}$ and
$T_{\text{eff}} \leq 65 \text{ mK}$. The transmon excited-state populations in these experiments are measured by the protocol in Ref. [40] and listed in Table III.

To verify the efficacy of these cavity attenuators, we further performed two control experiments. First, in the same geometry as the 75-μm-gap copper attenuator, we machined an aluminum cavity. It becomes a lossless cavity filter below 1 K and thus should leave the thermal photon population of the readout mode unchanged. By coupling it to transmon A and performing the same temperature-dependent measurements, we acquired the yellow circles in Fig. 4. At 25 mK, we measured $T_{2e}/2T_1 = 0.75 \pm 0.06$, indicating $\bar{n}_{\text{th}} \leq 1 \times 10^{-3}$ and $T_{\text{eff}} \leq 55 \text{ mK}$, which are between the no-attenuator and brass/copper-attenuator results. Therefore, we conclude that the enhancement of qubit coherence in our cavity attenuator experiments is not only due to lossless filtering, which rejects the incoming thermal photons that would populate the higher modes of the readout cavity. Dissipation is necessary for reducing high-frequency dephasing noise caused by residual thermal photons in the readout mode.

As a second control, we repeated the copper-attenuator experiment but added to the aluminum readout cavity a copper coaxial cable coupler with coupling rate to the readout mode $\sim 5 \text{ kHz} \ll \kappa_c, \kappa_i$. This input line with 70 dB cold attenuation was terminated by a 50 Ω load at room temperature (see Fig. 8). At 25 mK, we observed $T_1 = 100 \pm 8 \mu$s, $T_{2e} = 171 \pm 10 \mu$s, and obtained $T_{2e}/2T_1 = 0.86 \pm 0.09$, $\bar{n}_{\text{th}} \leq 1 \times 10^{-3}$, corresponding to $T_{\text{eff}} \leq 55 \text{ mK}$ (data not shown in the Figures). We conclude that even a weakly coupled port has nongenligible contribution to qubit dephasing if it is not directly thermalized to the mixing chamber. Based on this and other experiments in our lab, we suspect in particular that the teflon in the coaxial cable is a source of excess photons. Therefore, to achieve the best qubit coherence, ideally every coupling port on the readout cavity should be properly protected by a cold cavity attenuator.

We tested the consistency of the performance of cavity attenuators by conducting experiments on the two transmons A and B in multiple cooldowns. Plotted in Fig. 5 are results with 300-μm-gap brass attenuators. These two cooldowns were separated by five months during which time the attenuators were removed from the setups. For both qubits, temperature-dependent measurements showed good reproducibility on $T_{2e}/2T_1$, which is close to 1 in average and larger than 0.9 within one standard deviation at base temperature. We believe that reliable performance of these attenuators arises from their well-understood materials, structure, and fabrication process.

FIG. 5. Consistency of $T_{2e}/2T_1$ across multiple samples and cooldowns when the qubits are protected by 300 μm brass cavity attenuators. For transmon B, $T_1 \approx 50 \pm 10 \mu$s below 100 mK.

IV. THERMAL PHOTON POPULATION MEASUREMENT

Precisely measuring $T_\phi$ and $\bar{n}_{\text{th}}$ becomes a challenging task when $T_2 \approx 2T_1$, as the fluctuation of $T_1$ over time causes the error bar of $\Gamma_\phi = 1/T_\phi$ to exceed $\Gamma_\phi$ itself. In order to mitigate the impact of the $T_1$ fluctuation on the determination of the residual $\bar{n}_{\text{th}}$, we performed noise-induced dephasing measurement on both transmons. Adopting a method similar to Refs. [22, 24], we amplitude-modulated broadband white noise (0–80 MHz) onto a continuous-wave microwave signal at the hybridized readout frequency. The total photon population in the readout mode becomes $n_{\text{tot}} = n_{\text{add}} + n_{\text{th}}$, in which $n_{\text{add}}$ is proportional to the output power of the noise generators. By measuring $n_{\text{tot}}$ as a function of the noise power (see Fig. 6), we can extract $n_{\text{th}}$ by linear regression. Finally, we obtained $n_{\text{th}} = 2(\pm 3/2) \times 10^{-4}$ for transmon A and $n_{\text{th}} = 2(\pm 4/2) \times 10^{-4}$ for transmon B when they are protected by copper cavity attenuators, corresponding to $T_{\text{eff}} \leq 44 \text{ mK}$. These results are consistent with the order-of-magnitude estimate in Sec. III, and lower than the values in two other recent reports [23, 24] that also aimed at reducing $\bar{n}_{\text{th}}$ in circuit QED systems.

V. DISCUSSION

The results of our experiments have two important implications: First, cavity attenuators can reproducibly reduce $\bar{n}_{\text{th}}$ of the readout cavity by an order of magnitude and extend $T_{2e}$ close to the $2T_1$ limit. Second, the improvement of qubit coherence by cavity attenuators is impacted if the readout cavity has any direct coupling to the input and output lines, even if the coupling is very weak. Our experiment suggests that excess thermal...
photons inevitably come from the commercial microwave components at base temperature. Consequently, cavity attenuators should be employed as a standard device to create a cold black body radiation environment for superconducting quantum circuits.

Two problems need to be solved before cavity attenuators can have broader applications in circuit QED experiments: First, in the experiments reported in this paper, qubit control and readout tones share the same coupling aperture protected by a cavity attenuator centered near the readout frequency. As a result, qubit control pulses are mostly filtered out, which slows down the qubit state manipulation. This can be avoided by separating the qubit control and readout ports and protecting them with cavity attenuators centered at different frequencies. More desirably, it is possible to design a multi-pole dissipative filter whose bandwidth covers a few qubits simultaneously. Second, in the current measurement setup, while dissipating excess thermal photons, the cavity attenuator also attenuates the readout signal. Consequently, the measurement signal-to-noise ratio is not sufficient for high-fidelity single-shot dispersive readout. This problem might be addressed by moving the cavity attenuator to the output port of the quantum-limited amplifier. More compactly, we could also realize in situ quantum-limited amplification in the readout cavity using Josephson junctions or ‘SNAILS’ [41–43]. Combined together, these solutions would bypass the conflict between the isolation and controllability of superconducting qubits, and therefore significantly enhance the qubit coherence times while retaining the benefits of strong qubit–photon interactions in artificial quantum circuits.

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Appendix A: Experimental Details

The two transmon qubit—A and B—measured in our experiments were fabricated with double-angle-evaporated Al/AlOx/Al Josephson junctions defined using the bridge-free electron-beam lithography technique [44, 45] on double-side-polished c-plane sapphire chips. As depicted in Fig. 7, the transmon is placed 6.9 mm away from the center of the 3D aluminum readout cavity—an antinode of the electric field of the TE103 mode whose coupling to the qubit is intended to be
minimized. The $\text{TE}_{101}$ mode of the readout cavity and the $\text{TE}_{001}$ mode of the cavity attenuator are hybridized through an aperture to form the readout mode, which is coupled to the input–output coaxial cable through a waveguide-to-SMA pin coupler. The frequency, $\kappa_i$, and $\kappa_c$ of the readout mode in various experiments are listed in Table III.

As shown in Fig. 8, the coupled cavities are housed in a $\mu$-metal (Amumetal A4K) magnetic shield with a carbon black copper plate inside and mounted to the mixing chamber stage of an Oxford Triton™ cryo-free dilution refrigerator. The combination of a K&L 12 GHz low-pass filter and a homemade Eccosorb filter is installed on every qubit input and output line on the base stage to block spurious radiations at high frequencies. The leftmost input line is terminated by a 50 Ω load at room temperature and connected to the aluminum readout cavity through a 5 kHz coupler only in the second control experiment reported in Sec. III. A “SNAIL” parametric amplifier (SPA) [42, 46] was used to collect part of the data sets. An array of three cryogenic circulators impose the directionality of the readout signals, which are transmitted in NbTi superconducting cables between the cavity attenuator and the SPA, as well as between the base stage and the 3.5 K stage along the output line. The output signals are further amplified by a high-electron-mobility transistor (HEMT) at 3.5 K and a combination of room-temperature amplifiers before being demodulated by a heterodyne interferometer and digitized by an analog-to-digital card in the measurement computer.

[1] M. H. Devoret and R. J. Schoelkopf, “Superconducting circuits for quantum information: An outlook,” Science 339, 1169 (2013).
[2] D. Vion, A. Aassime, A. Cottet, P. Joyez, H. Pothier, C. Urbina, D. Esteve, and M. H. Devoret, “Manipulating the quantum state of an electrical circuit,” Science 296, 886 (2002).
[3] A. Cottet, Implementation of a quantum bit in a superconducting circuit, PhD dissertation, Universite Paris VI (2002).
[4] J. Koch, T. M. Yu, J. Gambetta, A. A. Houck, D. I. Schuster, J. Majer, A. Blais, M. H. Devoret, S. M. Girvin, and R. J. Schoelkopf, “Charge-insensitive qubit design derived from the cooper pair box,” Phys. Rev. A 76, 042319 (2007).
[5] J. A. Schreier, A. A. Houck, J. Koch, D. I. Schuster, B. R. Johnson, J. M. Chow, J. M. Gambetta, J. Majer, L. Frunzio, M. H. Devoret, S. M. Girvin, and R. J. Schoelkopf, “ Suppressing charge noise decoherence in superconducting charge qubits,” Phys. Rev. B 77, 180502 (2008).
[6] J. Q. You, X. Hu, S. Ashhab, and F. Nori, “Low-decoherence flux qubit,” Phys. Rev. B 75, 140515 (2007).
[7] M. Steffen, S. Kumar, D. P. DiVincenzo, J. R. Rozen, G. A. Keefe, M. B. Rothwell, and M. B. Ketchen, “High-coherence hybrid superconducting qubit,” Phys. Rev. Lett. 105, 100502 (2010).
[8] V. E. Manucharyan, J. Koch, L. I. Glazman, and M. H. Devoret, “Fluxonium: Single cooper-pair circuit free of charge offsets,” Science 326, 113 (2009).
[9] A. Blais, R.-S. Huang, A. Wallraff, S. M. Girvin, and R. J. Schoelkopf, “Cavity quantum electrodynamics for superconducting electrical circuits: An architecture for quantum computation,” Phys. Rev. A 69, 062320 (2004).
[10] A. Wallraff, D. I. Schuster, A. Blais, L. Frunzio, R.-S. Huang, J. Majer, S. Kumar, S. M. Girvin, and R. J. Schoelkopf, “ Strong coupling of a single photon to a superconducting qubit using circuit quantum electrodynamics,” Nature 431, 162 (2004).
[11] D. Esteve, M. H. Devoret, and J. M. Martinis, “Effect of an arbitrary dissipative circuit on the quantum energy levels and tunneling of a Josephson junction,” Phys. Rev. B 34, 158 (1986).
G. Kirchmair, L. Frunzio, L. I. Glazman, S. M. Girvin, and R. J. Schoelkopf, “Photon shot noise dephasing in the strong-dispersive limit of circuit QED,” Phys. Rev. B 86, 180504 (2012).

[22] F. Yan, S. Gustavsson, A. Kamal, J. Birenbaum, A. P. Sears, D. Hover, T. J. Gudmundsen, D. Rosenberg, G. Samach, S. Weber, J. L. Yoder, T. P. Orlando, J. Clarke, A. J. Kerman, and W. D. Oliver, “The flux qubit revisited to enhance coherence and reproducibility,” Nat. Commun. 7, 12964 (2016).

[23] J.-H. Yeh, J. LeFebvre, S. Premaratne, F. C. Wellstood, and B. S. Palmer, “Microwave attenuators for use with quantum devices below 100 mK,” J. Appl. Phys. 121, 224501 (2017).

[24] F. Yan, D. Campbell, P. Krantz, M. Kjaergaard, D. Kim, J. L. Yoder, D. Hover, A. Sears, A. J. Kerman, T. P. Orlando, S. Gustavsson, and W. D. Oliver, “Distinguishing coherent and thermal photon noise in a circuit quantum electrodynamical system,” Phys. Rev. Lett. 120, 260501 (2018).

[25] J. Gambetta, A. Blais, D. I. Schuster, A. Wallraff, L. Frunzio, J. Majer, M. H. Devoret, S. M. Girvin, and R. J. Schoelkopf, “Qubit–photon interactions in a cavity: Measurement-induced dephasing and number splitting,” Phys. Rev. A 74, 042318 (2006).

[26] B. Suri, Z. K. Keane, R. Ruskov, L. S. Bishop, C. Tahan, S. Novikov, J. E. Robinson, F. C. Wellstood, and B. S. Palmer, “Observation of Autler-Townes effect in a dispersively dossed Jaynes–Cummings system,” New J. Phys. 15, 125007 (2013).

[27] C. Rigetti, J. M. Gambetta, S. Poletto, B. L. T. Plourde, J. M. Chow, A. D. Córcoles, J. A. Smolin, S. T. Merkel, J. R. Rozen, G. A. Keefe, M. B. Rothwell, M. B. Ketchen, and M. Steffen, “Superconducting qubit in a waveguide cavity with a coherence time approaching 0.1 ms,” Phys. Rev. B 86, 100506 (2012).

[28] J. Goetz, S. Pogorzalek, F. Deppe, K. G. Fedorov, P. Eder, M. Fischer, F. Wulschner, E. Xie, A. Marx, and R. Gross, “Photon statistics of propagating thermal microwaves,” Phys. Rev. Lett. 118, 103602 (2017).

[29] N. W. Ashcroft and N. D. Mermin, Solid State Physics (Cengage, Boston, 1976).

[30] M. L. Roukes, M. R. Freeman, R. S. Germain, R. C. Richardson, and M. B. Ketchen, “Hot electrons and energy transport in metals at millikelvin temperatures,” Phys. Rev. Lett. 55, 422 (1985).

[31] F. C. Wellstood, C. Urbina, and J. Clarke, “Hot-electron effects in metals,” Phys. Rev. B 49, 5942 (1994).

[32] D. M. Pozar, Microwave Engineering, 4th ed. (Wiley, Hoboken, 2012).

[33] K. H. Ho, S. T. Newman, S. Rahimifard, and R. D. Allen, “State of the art in wire electrical discharge machining (WEDM),” Int. J. Mach. Tools Manuf. 44, 1247 (2004).

[34] Wire EDM cutting was performed by the Gibbs Machine Shop at Yale University and the Advanced Research Corporation (ARC).

[35] T. Brecht, Y. Chu, C. Axline, W. Pfaff, J. Z. Blumoff, K. Chou, L. Krayzman, L. Frunzio, and R. J. Schoelkopf, “Micromachined integrated quantum circuit containing a superconducting qubit,” Phys. Rev. Applied 7, 044018 (2017).

[36] A. B. Pippard, “The surface impedance of superconductors and normal metals at high frequencies II. the anomalous skin effect in normal metals,” Proc. Roy. Soc. A 191, 385 (1947).

[37] R. G. Chambers, “Anomalous skin effect in metals,” Nature 165, 239 (1950).

[38] A. B. Pippard, “Metallic conduction at high frequencies and low temperatures,” in Advances in Electronics and Electron Physics, Vol. 6, edited by L. Marton (Academic Press, 1954) p. 1.

[39] M. D. Reed, B. R. Johnson, A. A. Houck, L. DiCarlo, J. M. Chow, D. I. Schuster, L. Frunzio, and R. J. Schoelkopf, “Fast reset and suppressing spontaneous emission of a superconducting qubit,” Appl. Phys. Lett. 96, 203110 (2010).

[40] K. Geerlings, Z. Leghtas, I. M. Pop, S. Shankar, L. Frunzio, R. J. Schoelkopf, M. Mirrahimi, and M. H. Devoret, “Demonstrating a driven reset protocol for a superconducting qubit,” Phys. Rev. Lett. 110, 120501 (2013).

[41] A. Narla, K. M. Sliwa, M. Hatridge, S. Shankar, L. Frunzio, R. J. Schoelkopf, and M. H. Devoret, “Wireless Josephson amplifier,” Appl. Phys. Lett. 104, 232605 (2014).

[42] N. E. Frattini, U. Vool, S. Shankar, A. Narla, K. M. Sliwa, and M. H. Devoret, “3-wave mixing Josephson dipole element,” Appl. Phys. Lett. 110, 222603 (2017).

[43] A. Eddins, J. M. Kreikebaum, D. M. Toyli, E. M. Levenson-Falk, A. Dove, W. P. Livingston, B. A. Levitan, L. C. G. Govia, A. A. Clerk, and I. Siddiqi, “High-efficiency measurement of an artificial atom embedded in a parametric amplifier,” (2018), arXiv:1806.05276.

[44] F. Lecocq, I. M. Pop, Z. Peng, I. Matei, T. Crozes, T. Fournier, C. Naud, W. Guichard, and O. Buisson, “Junction fabrication by shadow evaporation without a suspended bridge,” Nanotechnology 22, 315302 (2011).

[45] C. Rigetti, Quantum Gates for Superconducting Qubits, PhD dissertation, Yale University (2009).

[46] N. E. Frattini, V. V. Sivak, A. Lingenfelter, S. Shankar, and M. H. Devoret, “Optimizing the nonlinearity and dissipation of a SNAIL parametric amplifier for dynamic range,” Phys. Rev. Applied 10, 054020 (2018).
FIG. 8. Cryogenic wiring diagram with simplified room-temperature microwave electronics. The bottommost segment of the leftmost input line is dashed since it is only connected in the second control experiment reported in Sec. III.
TABLE III. Frequency $f_{ro}$, rates $\kappa_i$ and $\kappa_c$ of the readout mode, dispersive shift $\chi$, $T_{2e}/T_1$, estimated upper bounds of $\bar{n}_{th}$ and $T_{eff}$ at 25 mK, and transmon excited-state population $P_e$ for each experiment in Fig. 4. The $\kappa_i$'s for the experiments without an attenuator and with an aluminum filter are below fitting errors.

| Attenuator | Material Gap (µm) | $f_{ro}$ (GHz) | $\kappa_i/2\pi$ (MHz) | $\kappa_c/2\pi$ (MHz) | $T_{2e}/T_1$ | $\bar{n}_{th}$ | $T_{eff}$ (mK) | $P_e$ |
|------------|-------------------|-----------------|------------------------|------------------------|-------------|-------------|----------------|------|
| None       | n/a               | 7.573           | n/a                    | 16.5                   | 1.5         | $0.72 \pm 0.12$ | $\leq 4 \times 10^{-3}$ | $\leq 65$ | 0.01 |
| Al         | 75                | 7.847           | n/a                    | 0.24                   | 1.1         | $0.75 \pm 0.06$ | $\leq 1 \times 10^{-3}$ | $\leq 55$ | 0.01 |
| Brass      | 300               | 7.573           | 11.4                   | 1.9                    | 1.2         | $0.98 (+0.02/-0.08)$ | $\leq 2 \times 10^{-4}$ | $\leq 43$ | 0.005 |
| Cu         | 75                | 7.857           | 7.1                    | 0.9                    | 1.1         | $1.00 (+0.00/-0.12)$ | $\leq 2 \times 10^{-4}$ | $\leq 44$ | 0.04 |