An Overview of Fatigue Strength of Case-Hardening TRIP-Aided Martensitic Steels

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Abstract: Surface-hardened layer characteristics and fatigue strength properties of transformation-induced plasticity-aided martensitic steels subjected to heat-treatment or vacuum carburization followed by fine-particle peening are revealed for automotive applications specially for powertrain parts. The as-heat-treated steels without the case-hardening process possess excellent impact toughness and fatigue strength. When the steels are subjected to fine-particle peening after heat-treatment, the fatigue limits of smooth and notched specimens increase considerably, accompanied with low notch sensitivity. Vacuum carburization and subsequent fine-particle peening increases further the fatigue strength of the steels, except notch fatigue limit. The increased fatigue limits are principally associated with high Vickers hardness and compressive residual stress just below the surface, resulting from the severe plastic deformation and the strain-induced martensitic transformation of metastable retained austenite, as well as low surface roughness and fatigue crack initiation depth.

Keywords: TRIP-aided martensitic steel; case-hardening; vacuum carburization; fine-particle peening; fatigue strength

1. Introduction

Recently, four types of transformation-induced plasticity (TRIP)-aided steels with different matrix structures and different chemical compositions, namely “TRIP-aided bainitic ferrite (TBF) steel” [1–10], “TRIP-aided martensitic (TM) steel” [11–21], “quenching and partitioning (Q&P) steel” [22–31], and “medium Mn TRIP-aided steel” [32–39] have been developed as third-generation advanced high-strength steels (AHSSs) for automotive sheet products. These steels possess high toughness, fatigue strength and delayed fracture strength, as well as excellent cold formability, especially in TM steels [7,11,16–20]. Therefore, these steels are expected to be also a suitable material for high torque powertrain parts which are produced by cold and hot forging [40], in the same way as “nanostructured bainitic steel” [41–48].

Many researchers found that shot peening considerably increases the fatigue strength of the conventional case-hardening martensitic steels [49–59]. Sugimoto et al. [60–62] have reported that high fatigue strength and low notch-sensitivity for fatigue of the TM steel are achieved by fine-particle peening and/or vacuum carburization because of small surface roughness and the improved surface-hardened layer properties. In addition, they showed that further increase in fatigue limit of the steels is achieved by using of multi process of vacuum carburization and fine-particle peening which increases the hardness and residual stress in the surface hardened layer [63–65].
In this paper, microstructural properties (matrix, second phase and retained austenite characteristics), mechanical properties (tensile, impact and fatigue properties) and relationships between the microstructural and mechanical properties of as-heat-treated (0.1–0.6)%C–1.5%Si–1.5%Mn–Cr–Mo–Ni TM steels are first introduced to understand the internal characteristics of case-hardening TM steel. Next, surface-hardened layer properties and fatigue strength of 0.2%C–1.5%Si–1.5%Mn–1.0%Cr–(0–0.2)%Mo TM steels subjected to heat-treatment or vacuum-carburization followed by fine-particle peening are explained. Besides, the fatigue strength properties are mainly correlated with the Vickers hardness and the residual stress in the surface-hardened layer which are enhanced by the strain-induced martensite transformation of metastable retained austenite and severe plastic deformations, as well as the surface roughness and fatigue crack initiation depth. This review paper is based on our researches referring to the fatigue strength of TM steels because no researcher could identify and address potential issues.

2. As-Heat-Treated TM Steels

2.1. Microstructure

C–Si–Mn–Cr–Mo–Ni TM steels with tensile strength higher than 1470 MPa can be produced by the multi-step heat-treatment consisting of austenitization and subsequent isothermal transformation at temperature below martensite-finish temperature (\(M_f\)) shown in Figure 1 [11–21]. On cooling to the isothermal transformation temperature, most of the austenite first transforms to soft \(\alpha'\)-martensite with wide lath structure, with a small amount of untransformed austenite. On subsequent cooling after isothermal transformation, the austenite changes into a mixture of hard \(\alpha'\)-martensite with narrow lath structure and carbon-enriched retained austenite (MA)-like phase. Resultantly, microstructure of the TM steels principally consists of soft \(\alpha'\)-martensite matrix and MA-like phase (Figure 2) [13]. Most of the MA-like phases are located on prior austenitic grain, packet and block boundaries. The retained austenite phases are mainly filmy and in existence along narrow lath-martensite boundary in the MA-like phase, as shown in Figure 3. Fine and needle shaped carbides seem to precipitate only in wide lath-martensite structure. This means that the carbides are already precipitated during auto-tempering on quenching prior to low temperature isothermal transformation. It is noteworthy that the carbide fraction is much lower than that of the conventional low alloy martensitic steels with low content of Si.

![Multi-step heat-treatment diagram](image_url)

**Figure 1.** Multi-step heat-treatment diagram (austenitizing and subsequent isothermal transforming, followed by partitioning) of TM steel [16]. Isothermal transformation time is \(t_{IT} = 1000\) s. Subscripts “IT” and “P” denote isothermal transforming and partitioning, respectively. OQ: quenching in oil at 50 °C.
Figure 2. Phase maps of (a) 0.2%C–, (b) 0.4%C– and (c) 0.6%C–1.5%Si–1.5%Mn TM steels subjected to isothermal transforming at 50 °C for 1000 s after austenitizing [13]. Orange and yellowish green phases denote coarse lath-martensite ($\alpha_m$) and MA-like phase (MA), respectively. Dark green dots in MA-like phase are retained austenite ($\gamma_R$). $\alpha_m^*$ is narrow lath-martensite.

If isothermal transformation was conducted at low temperature such as room temperature, the retained austenite is not carbon-enriched sufficiently (is not stabilized mechanically). In this case, partitioning treatment at temperatures between $M_S$ and $M_f$ is usually employed after the isothermal transforming; the partitioning is different from the conventional low temperature tempering because it aims to carbon-enrichment into the retained austenite and soften further the soft $\alpha'$-martensite, without dissolution of the retained austenite and carbide precipitation [11,12,15].

Volume fractions of retained austenite and MA-like phase increase with increasing carbon content of steel and isothermal transformation temperature at temperatures between $M_S$ and $M_f$ [16,19]. In this case, carbide fraction decreases with increasing isothermal transformation temperature. At near $M_S$, no carbide precipitates in the wide lath-martensite, in the same way as bainitic ferrite. The carbon concentration of retained austenite is independent of isothermal transformation temperature and nearly constant. Partitioning at temperatures lower than 350 °C for 1000 s increases carbon concentration of retained austenite although partitioning higher than 250 °C reduces only a little retained austenite fraction with an increase of carbide fraction [11,17].

Figure 3. TEM image of 0.2%C–1.5%Si–1.5%Mn–1.0%Cr TM steel subjected to isothermal transforming at 50 °C for 1000 s [11]. $\alpha_m$: wide lath-martensite, MA: a mixture of narrow lath-martensite ($\alpha_m^*$) and filmy retained austenite ($\gamma_R$), $\theta$: carbide.
High carbon content increases the volume fractions of retained austenite and MA-like phase in (0.1–0.6)%C–1.5%Si–1.5%Mn TM steels with different carbon content (Figure 4). Higher carbon concentration of retained austenite can be obtained in the steels containing 0.2%C and 0.3%C [13,16]. The carbon concentration of retained austenite in 0.6%C steel is so much lower than the desired carbon content. This contradictory result may be due to large transformation strain of narrow lath-martensite. Microalloying of Cr, Mo, Ni and Mn also increases the volume fractions of retained austenite, MA-like phase and carbide, whereas decreases the carbon concentration of retained austenite [14,36].

**Figure 4.** Variations in (a) initial volume fraction ($f_{γ0}$) and carbon concentration ($C_{γ0}$) of retained austenite and (b) volume fractions of MA-like phase ($f_{MA}$) and carbide ($f_{θ}$) as a function of carbon content (C) in (0.1–0.6)%C–1.5%Si–1.5%Mn TM steels subjected to isothermal transforming at 50 °C for 1000 s (without partitioning) [13].

Sometimes, the steel subjected to isothermal transforming at temperatures between martensite-start temperature ($M_S$) and $M_f$ after austenitization is also regarded as TM steel because of similar microstructure [11] and mechanical properties [16], although the microstructure consists of soft $α′$-martensite/bainitic ferrite matrix and a larger amount of retained austenite than that of TM steel [11]. In this case, soft $α′$-martensite fraction can be estimated by using the empirical equation proposed by Koistinen and Marburger [66]. This multi-step heat-treatment resembles one-step Q&P process at temperatures between $M_S$ and $M_f$.

### 2.2. Tensile Properties

When isothermal transformation treatment is carried out at temperatures below $M_f$ in 0.2%C–1.5%Si–1.5%Mn–1.0%Cr–0.05%Nb TM steel, the tensile strength decreases and the total elongation increases with increasing isothermal transformation temperature [16]. In (0.1–0.6)%C–1.5%Si–1.5%Mn TM steels [13,16], the yield stress (or 0.2% offset proof stress) and tensile strength increase with increasing carbon content except for 0.6%C steel which fractures at an early stage (Figure 5). On the other hand, total and uniform elongations decrease with increasing carbon content. Resultantly, 0.4%C steel possesses the highest combination of tensile strength and total elongation ($TS \times TEl = 23$ GPa %). The notch-tensile strength tends to increase with increasing carbon content in the same way as tensile strength. TM steels with carbon content of 0.2% to 0.4% exhibit higher notch-strength ratio than 0.1%C steel due to high TRIP effect of the retained austenite. The high notch-strength ratios are the same as those of quenched and tempered JIS-SCM420, 435 and 440 steels (Cr-Mo steels with different carbon content) [13]. Additions of Cr, Mo, Ni and Mn to 0.2%C–1.5%Si–1.5%Mn TM steel increase the yield stress and tensile strength, but decrease the elongations. Optimum combination of tensile properties can be obtained for 1.0%Cr bearing TM steel [14,17].

Sugimoto et al. [17] proposed that high combination of tensile strength and total elongation of TM steel is associated with the following characteristic microstructures:

1. A soft wide lath-martensite matrix with only a little carbide and diluted carbon concentration which improves the ductility,
(2) a large quantity of finely dispersed MA-like phase which produces a large mean internal stress resulting from a difference in flow stress between a soft wide-lath martensite and a hard MA-like phase,

(3) a metastable retained austenite of 2–5 vol %, which increases hard strain-induced martensite fraction and plastically relaxes the localized stress concentration on strain-induced transformation.

Figure 5. Variations in (a) yield stress or 0.2% offset proof stress (YS), tensile strength (TS), notch tensile strength and notch strength ratio (NSR = TS/N/TS) and (b) uniform and total elongations (UEL and TEL) and product of TS and TEl (TS × TEl) as a function of carbon content (C) in (0.1–0.6)%C–1.5%Si–1.5%Mn TM steels [13]. Stress concentration factor of notched specimen is 1.9.

2.3. Impact Toughness

It can be seen that when 1%Cr, 1%Cr–0.2%Mo, or 1%Cr–0.2%Mo–1.5%Ni is added to the base steel with a chemical composition of 0.2%C, 1.5%Si, 1.5%Mn and 0.05%Nb, the TM steels exhibit high V-notched Charpy impact absorbed values at 25°C ranging between 100 to 125 J/cm², and low ductile-brittle transition temperatures (corresponding to 50% ductile fracture appearance on Charpy impact tests) ranging from −150 to −130 °C (Figure 6) [14,19]. Moreover, the steels also possess the tensile strengths of around 1.4 to 1.5 GPa. The impact properties are far superior to those of the conventional low alloy martensitic steel (SCM 420 steel), in the same way as TBF and tempered Q&P [31] steels. In addition, the transition temperatures are considerably lowered as compared to TBF, tempered Q&P [31] and SCM420 steel. From the load–displacement curves obtained by impact testing, it is found that high impact values of TM steels are mainly caused by the high crack propagation energy [14]. Partitioning at 300 °C for 1000 s after isothermal transforming increases further impact values [12,14].

Figure 6. Relationships between tensile strength (TS) and (a) Charpy impact absorbed value (CIAV) at 25°C and (b) ductile-brittle transition temperature (DBTT) for 0.2%C–1.5%Si–1.5%Mn–(0–1.0)%Cr–(0–0.2)%Mo–(0–1.5)%Ni–0.05%Nb TM steels (●) subjected to isothermal transforming at 200 °C, SCM420 steel tempered at T_T = 200 to 600 °C for 3600 s (▲) and TBF steels (□) [14]. The TBF steels have the same composition as TM steels and are subjected to isothermal transforming (or austempering) at 400 °C for 1000 s.
Figure 7 depicts the fracture mechanism of ductile and brittle impact fractures of TM steel [14]. In a case of ductile impact fracture, MA-like phases play an important role in suppressing the void initiation and promoting the preferential void growth at the MA-like phase/matrix interface (Figure 7a). In a case of brittle impact fracture, on the other hand, the MA-like phases also inhibit the initiation of cleavage cracking, as shown in Figure 7b, because they reduce the facet size of cleavage crack and the strain-induced transformation of the retained austenite relaxes plastically the localized stress concentration. With this, the superior impact properties of TM steel are believed to be caused by the characteristic microstructures such as (1), (2) and (3) mentioned in the last of Section 2.2.

![Illustrations showing (a) ductile and (b) brittle impact fractures for TM steel](image)

**Figure 7.** Illustrations showing (a) ductile and (b) brittle impact fractures for TM steel [14]. $\alpha_m$, $\alpha_m^*$, $\gamma_R$, and $\theta$ represent wide lath-martensite, narrow lath-martensite, retained austenite, and carbide, respectively. LC: quasi-cleavage crack path decided by the space between MA-like phases located on prior austenitic grain, packet and block boundaries.

### 2.4. Fatigue Properties

TM steel exhibits large fatigue hardening with subsequent softening in the same way as TBF steel (Figure 8a) [2,3,8,20], although commercial low alloy martensitic steel (SCM420 steel) softens during the cyclic deformation. Regardless of the high stress amplitude, a longer failure time and a larger plastic strain amplitude than those of SCM420 steel are also observed in the TM steel (Figure 8b), although the plastic strain is smaller than that of TBF steel. This cyclic hardening is mainly caused by “mean internal stress hardening” and “transformation hardening” [20] which result from the characteristic microstructures such as (1), (2) and (3) mentioned in the last of Section 2.2.

![Variations in (a) stress amplitude ($\sigma$) and (b) plastic strain amplitude ($\Delta \varepsilon_p$) vs. the number of cycles (N) for 0.2%C–1.5%Si–1.5%Mn TM (●) and TBF (▲) steels, and SCM420 steel (▲) [20]. Tests were carried out under tension-compression mode with a stress ratio of −1. Strain amplitude range is $\Delta \varepsilon = 1.5\%$ and frequency is 1 Hz.](image)

**Figure 8.** Variations in (a) stress amplitude ($\sigma$) and (b) plastic strain amplitude ($\Delta \varepsilon_p$) vs. the number of cycles (N) for 0.2%C–1.5%Si–1.5%Mn TM (●) and TBF (▲) steels, and SCM420 steel (▲) [20]. Tests were carried out under tension-compression mode with a stress ratio of −1. Strain amplitude range is $\Delta \varepsilon = 1.5\%$ and frequency is 1 Hz.

Figure 9 shows fatigue limits of smooth and notched specimens of (0.1–0.6)%C–1.5%Si–1.5%Mn TM steels with different carbon content [13,19] and the “notch-sensitivity factor $q$” [67] defined by the following equation,

$$q = (K_t - 1)/(K_t - 1) \quad (1)$$
where $K_f$ and $K_t$ are fatigue-notch factor (=$\sigma_w/\sigma_{wn}$; $\sigma_w$, $\sigma_{wn}$: fatigue limits of smooth and notched specimens, respectively) and stress concentration factor (1.9 in this study), respectively. Both fatigue limits of smooth and notched specimens increase with increasing carbon content in steels between 0.1% C and 0.4% C. The notch-sensitivity factor is the minimum in 0.3% C steel. Notched fatigue limits of the steels containing 0.2% C to 0.4% C are higher than those of SCM420, 435 and 440 steels with different carbon content. The notch-sensitivity factors of the TM steels are lower than those of SCM420, 435 and 440 steels. However, TBF steels possess relatively higher notch fatigue limits and far lower notch sensitivity factor than TM steels [7]. Similar tendency is also reported for fatigue limits in Q&P steels [24, 27, 28, 41].

In general, fatigue limits of smooth and notched specimens are principally controlled by fatigue crack initiation and propagation stages, respectively. Figure 10a shows a SEM image illustrating a fatigue crack initiated on the surface of a notched specimen of TM steel [13]. According to Knott [68], the plastic zone size $d_Y$ of crack tip under plane strain condition (Figure 10b) can be estimated from the following equation:

$$d_Y = K^2 / (6\pi Y S^2)$$  

where $YS$ is the yield stress, and $K$ is the stress intensity factor defined as $\sigma (\pi c)^{1/2}$, $\sigma$ is the applied stress, and $c$ is the crack length. From Figure 10a, it appears that the fatigue crack initiates in the wide lath martensite structure and is stopped at the MA-like phase [13]. In the 0.4% C steel, the plastic zone size is estimated to be about 2.0 $\mu$m if the fatigue crack length at the first stage is $2c = 30 \mu$m, equivalent to the prior austenitic grain size, and the applied stress is corresponding to the fatigue limit. The plastic zone always includes some retained austenite particles in MA-like phase (see Figure 10b) because the interparticle path of MA-like phase is 0.5 to 2.0 $\mu$m (Figure 2b). Therefore, the plastic relaxation by the strain-induced transformation of retained austenite can be expected to take place always in the plastic zone during fatigue deformation. In conclusion, the high notch fatigue limits of TM steels can be considered to be principally caused by an increase in volume fraction of hard phase, plastic relaxation and crack closure via the strain-induced martensite transformation of metastable retained austenite, as well as a very small amount of carbide. Tomita et al. [41] also reports the similar improving mechanism for fatigue strength in 0.6% C–1.5% Si–0.8% Mn steel.

It is very difficult to compare the fatigue limits of TM steels with other AHSSs because fatigue tests are not conducted under the same fatigue mode and stress ratio. However, from comparison of several references [1, 4, 6, 7, 9, 27, 28, 41, 42, 44–48], we can conclude that TM steels possess the high fatigue limits compared to the conventional quenched and tempered martensitic steels, in the same
way as several AHSSs such as TBF steels [1,4,6,7,9], Q&P steels [27,28] and nanostructured bainitic steels [41,42,44–49].

Figure 10. (a) SEM image of the initial crack formed on the surface of notched specimen in 0.4%C–1.5%Si–1.5%Mn TM steel, fractured at \( N_f = 5.0 \times 10^4 \) cycles under tension-tension mode (a stress ratio of 0.1) at 25 ℃ with a sinusoidal wave of 80 Hz [13]. (b) An illustration of the plastic zone size \( (b_Y) \) in TM steel depicting the crack tip and distribution of MA-like phases: where \( \alpha_m, \alpha_m^* \), \( \gamma_R \), \( \theta \) and MA represent wide lath-martensite, narrow lath-martensite, retained austenite, carbide and MA-like phase, respectively.

3. Heat-Treated and Subsequently Fine-Particle Peened TM Steels

3.1. Surface-Hardened Layer Properties

When heat-treated 0.2%C–1.5%Si–1.5%Mn–1.0%Cr TM and JIS-SNCM420 steels (0.2%C–0.2%Si–0.5%Mn–0.6%Cr–0.2%Mo–1.7%Ni, quenched and tempered at 200 ℃ for 3600 s) are subjected to fine-particle peening under arc-height of 0.104 mm (N) at room temperature [62], the microstructures just below the surface are considerably refined and severely deformed without white layer (a nanosized or amorphous structure) [69], in the same way as TBF steel [60,61] (Figure 11b,d). In this case, arc-height of fine-particle peening under arc-height of 0.104 mm (N) is quantified using Almen strip of N type and the coverage is 300%. The maximum roughness height (Rz, JIS B0601:2001) on the surface of both steels is less than 4 μm because of the use of the small shot particles (steel ball of 70 μm diameter) (Figure 11a,c).

Figure 11. SEM images of (a,c) top-view of surface and (b,d) cross-sectional side view of surface-hardened layer of the smooth specimens of (a,b) heat-treated 0.2%C–1.5%Si–1.5%Mn–1.0%Cr TM and (c,d) SNCM420 steels subjected to fine-particle peening under arc-height of 0.104 mm (N) [62]. Maximum roughness heights of the TM and SNCM420 steels are Rz = 3.85 and 3.76 μm, respectively.

The distributions of Vickers hardness, volume fraction of untransformed retained austenite, and X-ray residual stress of the \( \alpha \) (bcc) phase in the surface-hardened layer of the TM and SNCM420 steel specimens are shown in Figure 12 [62]. The depth of the surface-hardened layer before fatigue testing is approximately 20 μm in both steels; the maximum Vickers hardness increment (ΔHV,
see Figure 12a) of the TM steel is larger than that of the SNCM420 steel. Most of the retained austenite transforms to martensite near the surface (Figure 12b). The ratio of the ΔHV to HV₀ (initial Vickers hardness, see Figure 12a) of TM steel increases with increasing volume fraction of strain-induced martensite (Δfαm), in the same manner as that of the TBF steel (Figure 13a) [61]. High compressive residual stresses occur in the α(bcc) phase of both steels before fatigue testing (Figure 12c). The compressive residual stress of the TM steel is larger than that of the SNCM420 steel. Maximum compressive residual stresses before fatigue are obtained at a depth of approximately 5–10 µm from the surface in both steels.

The maximum Vickers hardness and maximum compressive residual stress increase with increasing Δfαm (Figure 13a,b). This indicates that the differences in Vickers hardness and compressive residual stress between both steels result from the differences in the Δfαm. The difference in the compressive residual stress is also associated with the expansion strain that occurs on the strain-induced martensite transformation. After fatigue tests at the stress amplitude corresponding to fatigue limit, the surface-hardened layer is considerably softened in both steels (Figure 12a), with a slight decrease in the retained austenite fraction (Figure 12b). In particular, the Vickers hardness in the surface-hardened layer of SNCM420 steel is much lower than the original Vickers hardness. This behavior resembles cyclic softening of Figure 8a. It is noteworthy that the Vickers hardness of the TM steel increases even interior of the surface-hardened layer after fatigue deformation. Significant decreases in the compressive residual stress occur in both steels after fatigue test, although the compressive residual stress of the TM steel was slightly higher than that of SNCM420 steel (Figure 12c).

![Figure 12](image-url)

**Figure 12.** Distributions of (a) Vickers hardness (HV), (b) volume fraction of untransformed retained austenite (fo) and (c) residual stress of the α(bcc) phase (σαXα) as a function of depth from the surface (ds) in heat-treated TM (○●) and SNCM420 (▲●) steels subjected to fine-particle peening under arc-height of 0.104 mm (N) before (solid marks) and after (open marks) fatigue testing [62]. Stress amplitudes (σa) of fatigue tests correspond to fatigue limits (TM: σa = 919 MPa; SNCM420: σa = 872 MPa).

### 3.2. Fatigue Strength

Heat-treated TM steel subjected to fine-particle peening under arc-height of 0.104 mm (N) achieves higher fatigue limits than SNCM420 steel, especially for the notched specimen (Figure 14). The TM steel also exhibits lower notch sensitivity factor q than the SNCM420 steel, although the q value for unpeened TM steel is higher than that for unpeened SNCM420 steel. It is considered that the fatigue limits of smooth and notched specimens in both steels are apparently enhanced by Δfαm, because the
fatigue limits increase with increasing $\Delta f_{\alpha m}$ (Figure 13c) [62]. In Figure 13c, fatigue limits of SNCM420 steel tempered at 430 °C are added for the purpose of reference.

![Figure 13](image-url)

Figure 13. Variations in (a) hardness increment normalized to original hardness ($\Delta H/V/HV_0$), (b) maximum compressive residual stress before and after fatigue normalized to yield stress ($-\sigma_{\alpha,\text{max}}/YS$), and (c) fatigue limits of smooth and notched specimens ($\sigma_w$, $\sigma_{wn}$) as a function of the volume fraction of strain-induced transformed hard martensite ($\Delta f_{\alpha m}$) in 0.2%C–1.5%Si–1.5%Mn–1.0%Cr TM and TBF steels and SNCM420 steel subjected to fine-particle peening [62]. Fatigue limits of (c) were measured by rotary bending fatigue tests at 25 °C, using a sinusoidal wave of 3000 rpm and a stress ratio of $R = -1$. Marks $\triangle$ in (c) denote the fatigue limits of SNCM420 steel tempered at 430 °C.

![Figure 14](image-url)

Figure 14. Stress amplitude–number of cycles ($\sigma-N$) curves for (a) smooth and (b) notched specimens in 0.2%C–1.5%Si–1.5%Mn–1.0%Cr TM and SNCM420 steels subjected to fine-particle peening (FPP) under arc-height of 0.104 mm (N) and also under unpeened (UP) conditions [62]. Fatigue tests were conducted on a rotating bending fatigue testing machine at 25 °C, using a sinusoidal wave of 3000 rpm and a stress ratio of $R = -1$.

Matsui et al. [55] reported that the sum of estimated yield stress ($\sigma_{Y,\text{est}}$) and the absolute value of maximum compressive residual stress of $\alpha$(bcc) phase ($|\sigma_{\alpha,\text{max}}|$) is related to the fatigue limit in JIS-SCM822H steel (0.22%C–0.27%Si–0.74%Mn–0.17%Cu–0.06%Ni–1.09%Cr–0.36%Mo) subjected to shot peening under arc-heights of 0.30 mm (N), 0.55 mm (A) and 0.25 mm (C) after gas-carburizing, as follows:

$$\sigma_w = 0.3891 \times (\sigma_{Y,\text{est}} + |\sigma_{\alpha,\text{max}}|).$$

(3)
The value of $\sigma_{Y,\text{est}}$ can be estimated from $HV_{\text{max}}$ by:

$$
\sigma_{Y,\text{est}} = \frac{HV_{\text{max}}}{3} \times 9.80665 \times \left(\frac{YS}{TS}\right),
$$

(4)

where $YS/TS$ is the yield ratio (assumed by Matsui et al. [55] to be 0.95).

The relationships between fatigue limits of smooth and notched specimens ($\sigma_w$ and $\sigma_{wn}$) and $\sigma_{Y,\text{est}} + |\sigma_{X,\alpha,\text{max}}|$ for the TM and SNCM420 steels are shown in Figure 15 [62]. The $\sigma_w$s of the TM and SNCM420 steels exhibit the same relationship as those by Matsui et al. [55], despite no carburizing. For a case of notched specimen of both steels, the following empirical equation is found:

$$
\sigma_{wn} = 0.2282 \times (\sigma_{Y,\text{est}} + |\sigma_{X,\alpha,\text{max}}|).
$$

(5)

**Figure 15.** Relationship between the sum of estimated yield stress and maximum compressive residual stress ($\sigma_{Y,\text{est}} + |\sigma_{X,\alpha,\text{max}}|$), and rotary bending fatigue limits ($\sigma_w$, $\sigma_{wn}$) for smooth and notched specimens of 0.2%C–1.5%Si–1.5%Mn–1.0%Cr TBF and TM steels and SNCM420 steel subjected to fine-particle peening under arc-height of 0.104 mm (N) [62].

4. Vacuum-Carburized and Subsequently Fine-Particle Peened TM Steels

4.1. Surface-Hardened Layer Properties

The surface hardened layer of 0.2%C–1.5%Si–1.5%Mn–1.0%Cr–0.2%Mo TM steel subjected to vacuum carburization under carbon potential of 0.8 mass% contains a large amount of retained austenite and a small amount of the MA-like phase, although coarsened microstructure appears near the surface (Figure 16a) [63]. The retained austenite fraction achieves to the maximum value (20.5 vol %) at a depth of 50 µm (Figure 17a). Two types of retained austenite, i.e., an island type in the matrix and a filmy type in the MA-like phase, appear in the steels (Figure 16a). A majority of the MA-like phase seems to be clustered along the prior austenitic, packet, and block boundaries. Vickers hardness of the as-vacuum-carburized TM steel is 713 at maximum (Figure 17c) and residual stress of $\alpha$(bcc) phase is about −100 MPa (Figure 17e).
Figure 16. (a) EBSD phase map of 0.2%C–1.5%Si–1.5%Mn–1.0%Cr–0.2%Mo TM steel specimen subjected to vacuum carburization under carbon potential of 0.8 mass% and (b) SEM image of cross-sectional side view of surface-hardened layer and (c) optical image of surface of TM steel subjected to vacuum carburization and subsequent fine-particle peening under arc-height of 0.21 mm (N) by using steel ball of 50 µm [63,64]. Yellowish-green, red and gray regions represent α’-martensite (αm) matrix, retained austenite (γR) phase and martensite-austenite (MA)-like phase, respectively. In (c), maximum roughness height of surface is $R_z = 5.1 \mu m$.

Figure 17. Distributions of (a,b) volume fractions of retained austenite ($f_{\gamma}$), (c,d) Vickers hardness (HV), and (e,f) residual stress of the α(bcc) phase ($\sigma_{X\alpha}$) before (●) and after (○) fatigue test in vacuum-carburized 0.2%C–1.5%Si–1.5%Mn–1.0%Cr–0.2%Mo TM steel subjected to vacuum-carburizing (VC) and then fine-particle peening (FPP) under arc-height of 0.21 mm (N) (a,c,e) and 1.12 mm (N) (b,d,f) [63,64]. Black open marks (○) and lines represent the surface-hardened layer properties of the as-vacuum-carburized steel. The x-axis shows the depth from the surface in mm.
After fine-particle peening, maximum roughness height of vacuum-carburized TM steel increases with increasing arc-height (Figure 18b), although the surface roughness is nearly the same under arc-heights lower than 0.21 mm (N). The typical surface image is shown in Figure 16c. White layer [69], which plays an important role in the fatigue strength and wear resistance is formed on the surface of the vacuum-carburized TM steel subjected to fine-particle peening under arc-heights higher than 0.41 mm (N). A distinct white layer is not formed on the surface in case of arc-heights lower than 0.21 mm (N) (Figure 16b). In the vacuum-carburized TM steel subjected to fine-particle peening under arc-height lower than 0.21 mm (N), the maximum retained austenite fraction is obtained at a depth of 50 μm (Figure 17a). The maximum Vickers hardness and the maximum compressive residual stress are attained at the depths of 10–50 μm. It is noteworthy that the Vickers hardness and compressive residual stress attain to the maximum values on surface or at near surface, as well as a large amount of untransformed retained austenite, when fine-particle peening is conducted under arc-height of 0.104 and 0.21 mm (N) (Figure 17c,e). The depths referring to their maximum values increase with increasing arc-height for the fine-particle peening (Figure 17b,d,f). In a case of higher arc-height, a larger amount of the retained austenite transforms to martensite (Figure 17b).

In vacuum-carburized TM and SNCM420 steels, the maximum volume fraction of retained austenite decreases with increasing arc-height (Figure 18a). On the other hand, the maximum Vickers hardness, the maximum residual stress and the maximum roughness height increase with increasing arc-height (Figure 18). The TM steel exhibits higher retained austenite fraction and compressive residual stress compared with SNCM420 steel, although the maximum Vickers hardness of both steels is almost the same. According to Sugimoto et al. [63], the maximum Vickers hardness and the maximum residual stress are mainly developed by severe plastic deformation, with a small contribution of the strain-induced martensitic transformation of the retained austenite.

![Figure 18. Variations in (a) the maximum retained austenite fraction ($f_{\gamma,max}$) and the maximum Vickers hardness ($H_{V,max}$) and (b) the maximum compressive residual stress ($\sigma_{\alpha,max}$) and maximum roughness height ($R_z$) as a function of arc-height (AH) in TM (●) and SNCM420 (▲) steels subjected to vacuum-carburizing and subsequent fine-particle peening [63].](image)

### 4.2. Fatigue Properties

When vacuum-carburized TM and SNCM420 steels were subjected to fine-particle peening under arc-height of 0.21 mm (N), the fatigue limits of both steels exhibit the maximum values in an arc-height range of 0.104 to 1.22 mm (N) (Figure 19a) [64]. Moreover, the values of fatigue limit of both steels are similar, except for the fatigue limits of the vacuum-carburized steels. Kato et al. [53] also reported that the same arc-height achieved the highest fatigue limit in gas-carburized SCM822H steel (0.20%C–0.20%Si–0.75%Mn–0.15%Cu–0.10%Ni–1.10%Cr–0.15%Mo). The maximum increment in the fatigue limit ($\Delta\sigma_w$ in Figure 19a) and the percentage increase of vacuum-carburized TM steel due to fine-particle peening are 574 MPa and 82% at maximum, respectively. By the comparison of the fatigue limits with those [62] of heat-treated TM steels subjected to fine-particle peening under arc-height of 0.104 mm (N), the increase in the fatigue limit ($\Delta\sigma_w = 440$ MPa) is greater than that ($\Delta\sigma_w = 244$ MPa) of
heat-treated steels (Figure 19a). The increase in the fatigue limit is greater than those of gas-carburized martensitic steel subjected to shot peening or fine particle peening [57]. The optimum arc-height value for fatigue limit may vary if fine-particle peening is conducted under different shot material, angle of attack, velocity, etc. According to Sugimoto et al. [65], vacuum carburization followed by fine-particle peening increases notch sensitivity factor for fatigue because only few increase in the notch fatigue limit is obtained compared to that of smooth specimen.

During fatigue deformation, a large amount of untransformed retained austenite transforms to martensite in vacuum-carburized TM steel subjected to fine-particle peening under low arc-height (Figure 17a). According to study [62] using heat-treated TM steel (containing retained austenite fraction of 3.1 vol %) subjected to fine-particle peening under the arc-height of 0.104 mm (N), the Vickers hardness and the residual stress in the surface-hardened layer considerably decreased during a fatigue test at a stress amplitude corresponding to the fatigue limit. In this study, however, their declines are relatively slight and the Vickers hardness at a depth of more than 50 μm increases during fatigue deformation in vacuum-carburized TM steel subjected to fine particle peening under arc-height of 0.21 mm (N) (Figure 17c). The strain-induced martensite fraction during fatigue deformation of vacuum-carburized and fine-particle peened TM steel is far higher than that of heat-treated TM steel subjected to fine particle peening (Figure 17a). Therefore, this result indicates that the strain-induced martensite transformation of a large amount of untransformed retained austenite during fatigue deformation compensates large decreases in Vickers hardness and compressive residual stress and highly maintains the properties during fatigue deformation. Resultantly, the small declines of the Vickers hardness and compressive residual stress during fatigue deformation is considered to increase considerably the fatigue limit.

![Figure 19. Variations in (a) the fatigue limit (σ_f) and (b) the depth of crack origin from the surface (d_f) as a function of the arc-height (AH) in TM (●) and SNCM420 (▲) steels subjected to vacuum-carburizing and fine-particle peening (VC+FPP) [64]. In (a), marks ○ and △ represent fatigue limits of TM (original retained austenite fraction f_{γ0} = 3.2 vol %) and SNCM420 (f_{γ0} = 1.6 vol %) steels subjected to heat-treatment and fine-particle peening (HT+FPP), respectively. (I): increases in Vickers hardness and compressive residual stress, (II): fish-eye crack fracture at a high depth and very few strain-induced martensite transformation. Fatigue tests were conducted on a rotating bending fatigue testing machine at 25 °C, using a sinusoidal wave of 3000 rpm and a stress ratio of R = −1.

In Figure 20, the fatigue limits of vacuum-carburized TM steel subjected to fine-particle peening under the arc-height of 0.104 and 0.21 mm (N) reduce by decline (ii), compared to those of heat-treated TM steel although they linearly increase with increasing σ_{Y,est} + σ_{κ, max} (line (i)). Meanwhile, the fatigue limits under arc-height of 0.41 and 1.12 mm (N) shift down by decline (iii), despite higher maximum Vickers hardness and maximum compressive residual stress in the surface-hardened layer than those under lower arc-height. Sugimoto et al. [64] explain the declines (ii) and (iii) as follows.

The declines in fatigue limits of vacuum-carburized TM steel are related to the depth of fish-eye crack from surface because most of the fatigue failure occurs by fish-eye cracks (Figure 21), different from that of heat-treated TM steel [62]. The fish-eye crack depth increases with increasing arc-height of
fine-particle peening (Figures 19b and 21). Therefore, decline (ii) in fatigue limit is considered to be caused by fish eye fracture. Decline (iii) in fatigue limits is associated with deep fish-eye fracture and a small amount of strain-induced martensite transformation during fatigue deformation (Figure 17b). In this case, superior surface-hardened layer properties and a white layer formed by fine particle peening under the arc-height higher than 0.41 mm (N) hardly contribute to increase the fatigue limit (Figure 21b), although a little strain-induced martensite plays a role in slight plastic relaxation of the localized stress concentration [70].

\[ \sigma_w = 0.3891 \times \{ \sigma_{Y,est} + |\sigma_{X,\alpha,max}| \} \]  

\[ \sigma_w = 0.2917 \times \{ \sigma_{Y,est} + |\sigma_{X,\alpha,max}| \} \]  

\( \sigma_{Y,est} \) of vacuum-carburized and subsequently fine-particle peened steels, (ii): fish-eye crack fracture at a low depth, (iii): fish-eye crack fracture at a high depth and very few strain-induced transformation during fatigue deformation. HT+FPP: heat-treatment plus subsequent fine particle peening.

Figure 20. Relationship between the rotary bending fatigue limit (\( \sigma_w \)) and the sum of estimated yield stress and absolute value of maximum compressive residual stress (\( \sigma_{Y,est} + |\sigma_{X,\alpha,max}| \)) of TM (●) and SNCFM420 (▲) steels subjected to vacuum-carburizing and subsequent fine-particle peening [64]. (i): \( \sigma_w \) of vacuum-carburized and subsequently fine-particle peened steels, (ii): fish-eye crack fracture at a low depth, (iii): fish-eye crack fracture at a high depth and very few strain-induced transformation during fatigue deformation. HT+FPP: heat-treatment plus subsequent fine particle peening.

Figure 21. Distributions of surface-hardened layer properties and illustrations of initiation and propagation stages of fish-eye cracks in the vacuum-carburized TM steel subjected to fine-particle peening under arc-heights of (a) 0.104 and 0.21 mm (N) and (b) 0.41 and 1.12 mm (N) [64]. \( f_Y \): volume fraction of retained austenite; HV: Vickers hardness; \( |\sigma_{X,\alpha,max}| \): absolute value of residual stress in the \( \alpha \) (bcc) phase.

5. Conclusions  

The as-heat-treated TM steels possessed excellent impact toughness (high Charpy impact absorbed value and low ductile-brittle transition temperature) and high fatigue strength (large cyclic softening, high fatigue limit and low notch-sensitivity). When the steels are subjected to fine-particle peening after heat-treatment, the fatigue limits of smooth and notched specimens increased considerably, accompanied with low notch sensitivity. Vacuum carburization and subsequent fine-particle peening increased further the fatigue strength of the steels, except notch fatigue limit. The increased fatigue limits were principally associated with high Vickers hardness and compressive residual stress just
below the surface, resulting from the severe plastic deformation and the strain-induced martensitic transformation of metastable retained austenite, as well as low surface roughness and fatigue crack initiation depth.

Further increases in the mechanical properties are possible by hot-forging prior to case-hardening, which brings on an increase in retained austenite fraction and a refined microstructure. Resultantly, the hot-forging is expected to improve the toughness and fatigue strength [12,15,18], in the same way as TBF steels [71–73]. The use of C, Cr and Mo bearing TM steels makes easy to manufacture the hot-forged parts as drivetrains, Diesel engine common rail systems, and others [40] and resultantly achieve the lightweight and low fuel consumption, instead of conventional high-strength low alloy steels. It is greatly hoped that many researchers interest in the hot-forging of TM steel and investigate the mechanical properties, such as fatigue strength, toughness and wear property of the case-hardening hot-forging products.

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