Ultrafast asymmetric Rosen-Zener-like coherent phonon responses observed in silicon

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We investigate the spectral profiles of time signals attributed to coherent phonon generation in an undoped Si crystal. Here, the retarded longitudinal-optical (LO) phonon Green function relevant to the temporal variance of induced charge density of ionic cores is calculated by employing the polaronic quasiparticle model developed by the authors [Y. Watanabe et al., Phys. Rev. B 95, 014301 (2017); ibid., 96, 125204 (2017)]. The spectral asymmetry is revealed in the frequency domain of the signals under the condition that an LO phonon mode stays almost energetically resonant with a plasmon mode in the early time region; this lasts for approximately 100 fs immediately after the irradiation of an ultrashort pump-laser pulse. It is understood that based on the adiabatic picture in time, this asymmetry is caused by the Rosen-Zener coupling between both modes. The associated experimental results are obtained by measuring time-dependent electro-optic reflectivity signals, and it is proved that these are in harmony with the calculated ones. The spectra become more symmetric, as the photoexcited carrier density further changes from that meeting the above condition to higher and lower sides of carrier densities. Moreover, the effect of optical nutation of carrier density on the CP signals is addressed, and the present results are compared with the asymmetry caused by transient Fano resonance, and the spectral profiles observed in a GaAs crystal in the text.

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I. INTRODUCTION

Using ultrafast laser pulse irradiation to semiconductors, it is possible to impulsively generate bare particles, e.g., phonons, and observe their subsequent dressing by the many-body interactions, that is, formation of a quasiparticle. The use of quasiparticles in semiconductors may revolutionize modern semiconductor-based optical and electronic devise technologies, such as quantum computing. Coherent phonon (CP) generation induced by an ultrashort pulse laser has been investigated in various materials, and efforts of exploration in this research area have been devoted to the understanding of the underlying microscopic mechanism governing the CP generation and the concomitant quantum mechanical effects just after the pulse-irradiation. The experimental results of the CP generation have been examined on the basis of the two well-known classical models subject to a damped forced-oscillation: the impulsive stimulated Raman scattering model and the displacive excitation of CP model. These models succeed in part in demonstrating the qualitative features of the CP oscillation. However, such an approach is confronted with difficulties in describing the early stage of the CP generation dynamics that is governed by an interaction of strongly photoexcited carriers with longitudinal optical (LO) phonons. Hereafter, this stage is termed as the early time region (ETR), which lasts up to approximately 100 fs after the irradiation of pump-pulse. Actually, it is commonly observed in the ETR in experiments that oscillatory patterns of transient electro-optic reflectivity signals for the CP are largely deviated from signals observed in the temporal region following the ETR; this is termed hereafter as the classical region.

Such anomalous signals sharply distinguished from a damped harmonics are considered to result from certain quantum-mechanical effects. There have been few studies toward the understanding of the anomaly so far, aside from the exploration of coherent coupling usually related to nonlinear optical effects of four-wave mixing due to pumping and probing radiation. Transient Fano resonance observed in lightly n-doped Si is a vestige of the quantum-mechanical effects though not observed in polar-semiconductors such as GaAs and GaP. The manifestation of this effect is understood based on the polaronic quasiparticle (PQ) model, where photoexcited carriers are dressed in LO phonons by means of a strong coupling between these two particles in the ETR. A classical Fano oscillator model derived from the Fano-Anderson Hamiltonian is also applied for this experimental result. Further, based on the above PQ model, the following two effects are revealed. One is a different quantum-mechanical effect of transient plasmon-LO-phonon resonance, that is energetically resonant interaction of the plasmon with the LO phonon via dynamically screened Coulomb interaction, which causes irregular o-
In this paper, we delve deeper into the issue of the transient plasmon-LO-phonon resonance. The aim of it is to examine how the formation of such resonance affects the degree of asymmetry of the spectral profiles associated with the CP time signals by means of both theory and experiment. The spectral asymmetry is still one of the significant subjects in the study of the CP, and the transient Fano resonance mentioned above has been explored thus far exclusively on the view of the understanding of this subject. Here, based on the adiabatic picture with respect to time that is incorporated in the PQ model, the transient dynamics of the CP generation is described in terms of adiabatic energy curves of particles participating in this dynamics. A particular attention is paid to the curve-crossing behavior between the plasmon and the LO-phonon, and the origin of the discernible asymmetry is analyzed by virtue of the adiabatic two-state models, namely, the Landau-Zener (LZ) model and the Rosen-Zener (RZ) model, as is mentioned in more detail later. Also, the effect of optical nutation relevant to the above-mentioned Rabi flopping on the spectral asymmetry is taken into consideration.

This paper is organized as follows. The theoretical framework and the experimental setup are given in Sec. II and Sec. III, respectively. The results and discussion are given in Sec. IV, followed by the conclusions in Sec. V. Hereafter, atomic units (a.u.) are used throughout unless otherwise stated.

II. THEORY

The theoretical framework of the PQ model is surveyed. The more detail of it is already described in the previous papers. In short, the PQ model is a fully-quantum-mechanical model for the CP generation dynamics available for both of polar and non-polar semiconductors on an equal footing. The PQ operator is defined as composed of two kinds of operators; one is a quasiboson operator, given by a linear combination of a set of pairs of electron operators, and the other is an LO-phonon operator. Based on this PQ model, one can track the CP dynamics in the ETR. The total Hamiltonian of concern is composed of an electron Hamiltonian, an interaction between an electron and an external pump-pulse laser, an LO phonon Hamiltonian, and an electron-LO-phonon interaction. Here, a Coulomb potential interaction is incorporated with the electron Hamiltonian described by a two-band model including conduction (c) and valence (v) bands. The interaction of the laser with electron in band b at time t is given by

\[ \Omega_{bb}(t) = \Omega_{0bb}f(t) \cos \omega_0 t, \]

where \( \Omega_{0bb} \) represents the Rabi frequency, given by the product of peak electric-field strength of the laser pulse and the electric dipole moment between \( \Gamma \)-points of c and v bands. Here \( b \) is either c or v with \( b \neq b \), \( f(t) \) represents the pulse envelope function given by the Gaussian function with temporal width (the full width at half maximum) \( \tau_L \), and \( \omega_0 \) is the center frequency of the external laser-field. Hereafter, it is understood that creation and annihilation operators of electron with Bloch momentum \( k \) in band \( b \) are represented by \( a_{bk} \) and \( a_{bk}^\dagger \), respectively, and creation and annihilation operators of LO phonon with energy dispersion \( \omega_q \) at Bloch momentum \( q \) are represented by \( c_q^\dagger \) and \( c_q \), respectively.

We consider the time-evolution of a composite operator defined by

\[ A_q^b(kbb') = a_{bk}^\dagger a_{bk'}, \]

on the basis of adiabatic approximation with respect to \( t \), where \( A_q^b(kbb') \) represents a carrier density matrix for the transition from b-band to b-band with an anisotropic momentum distribution determined by the transferred momentum \( q \); this is quite small, but finite (\( q \neq 0 \)). Here, the rotating wave approximation is employed in order to remove high-frequency contributions from the equations of motion, and thus \( A_q^b(kbb') \) is replaced by

\[ A_q^b(kbb') = A_q^b(kbb') e^{-i\omega_q t}, \]

where \( \omega_{cv} = \omega_0, \omega_{vc} = -\omega_0 \), and \( \omega_0 = 0 \). Further a creation operator of a collective excitation mode — a plasmon — \( B^+_q \) with the plasma frequency \( \omega_{ppl} \) is introduced by a linear combination of the intraband density matrices \( A_q^b(kbb') \)'s. As regards the single-particle excitation mode, just the interband contributions from \( A_q^b(kbb') \)'s are retained, and the intraband contributions from \( A_q^b(kbb') \)'s are neglected because these vanish in the long wave-length limit \( (|q| \to 0) \).

The equations of motion of \( c_q^\dagger, c_q, A_q^b(kbb'), \) and \( B^+_q \) are provided in a matrix form of

\[ -i \frac{d}{dt} \begin{bmatrix} c_q^\dagger, A_q^b(kbb'), B^+_q \end{bmatrix} = \begin{bmatrix} c_q^\dagger, A_q^b(kbb'), B^+_q \end{bmatrix} \tilde{Z}_q. \]  (2)

Here, \( \tilde{Z}_q = \{ Z_{qqj} \} \) represents a non-Hermitian matrix, the explicit form of which is given in Ref. and hereafter, it is understood that \( j, j' = \{ pb, (kbb), pl \} \) with the LO-phonon mode \( pb \), the single-particle excitation mode \( (kbb) \), and the plasmon mode \( pl \). In Eq. (2), phenomenological damping constants for all of these modes are suppressed. In addition, the argument of \( t \) in \( c_q^\dagger, A_q^b(kbb'), B^+_q \), and \( \tilde{Z}_q \) is omitted just for the sake of simplicity, and hereafter this convention is used unless otherwise stated. Now, we introduce the PQ operator as follows:

\[ P^+_q = c_q^\dagger V^L_{qj} + B^+_q V^R_{qj} + \sum_{kb} A_q^b(kbb') V^R_{q(kbb')}, \]  (3)

where left and right eigenvalue problems of \( \tilde{Z}_q \) as \( V^L_{qj} Z_q = E_q V^L_{qj} \) and \( Z_q V^R = V^R E_q \), respectively, are solved in an adiabatic sense to obtain the \( j \)th eigenvalue \( E_{qj} \) and the corresponding biorthogonal set of eigenvectors \( \{ V^L_{qj}, V^R_{qj} \} \). The time-evolution of \( P^+_q \) is obtained...
by solving the associated Heisenberg equation, where a non-adiabatic coupling between \( j \)th and \( j' \)th modes are assumed negligibly small in the practical calculations.\(^{22}\)

In the linear response theory, the retarded phonon Green function \( D_R^R(t, t') \) indicates an induced charge density of ionic cores probed at time \( t' \) by a weak external potential with a delta-function form \( \delta(t') \). This is provided by \( D_R^R(t, t') = D_R^R(t, t') + [D_R^R(t, t')]^\ast \) in terms of the PQ operator with the relation of \( c_q^\dagger = \sum_j P_{qj}^\dagger V_{qj, ph}^L \) as follows:

\[
\begin{align*}
\check{D}_q^R(t, t') &= -i \langle [c_q(t), c_q^\dagger(t')] \rangle \delta(t - t') \\
&= -i \sum_{j,j'} V_{qph,j}^L(t) \left\langle \left[ P_{qj}^\dagger(t), P_{qj'}^\dagger(t') \right] \right\rangle \\
&\quad \times V_{qj', ph}^L(t') \delta(t - t')
\end{align*}
\]

(4)

and \( \check{D}_q^R(t, t') = \check{D}_q^R(t, t') \), where the ground-state expectation value is taken in \( \langle \cdots \rangle \). The induced charge density attributed to the CP generation is provided by

\[
Q_q(\tau) \equiv D_R^R(\tau + t', t') - D_R^{R(0)}(\tau + t', t')
\]

(5)

with \( \tau = t - t' \geq 0 \), and it is considered that \( Q_q(\tau) \) corresponds to a displacement function of the CP at time \( \tau \) side from an unimportant proportional constant. Here, the contribution of the incoherent phonon signal is subtracted, where this is given by the free phonon Green function \( D_R^{R(0)}(\tau + t', t') \) without the pump laser, and hereafter the probing time of \( t' = 0 \) is exclusively concerned. The oscillatory pattern of the CP is extracted by representing \( Q_q(\tau) \) as

\[
Q_q(\tau) = A_q(\tau) \cos [\Omega_q \tau + \Theta_q(\tau)]
\]

(6)

where \( \Theta_q(\tau) \) and \( A_q(\tau) \) represent a renormalized phase modulus \( \pi \) and a transitory amplitude at \( \tau \), respectively. The Fourier transform (FT) of \( Q_q(\tau) \) is provided by

\[
\check{Q}_q(\omega) = \int_0^\infty e^{-i\omega \tau} Q_q(\tau) d\tau,
\]

(7)

and the associated power spectrum \( S_q(\omega) \) is given by

\[
S_q(\omega) \propto |\check{Q}_q(\omega)|^2.
\]

(8)

In the long-time limit of \( \tau \) ensuring \( \tau \gg T_q \equiv 2\pi/\omega_q \), \( \Theta_q(\tau) \) and \( A_q(\tau) \) become \( \theta_q \) and \( A_q^0 \) \( e^{-\tau/T_{qph}} \), respectively, where \( \theta_q \) and \( A_q^0 \) are constants and \( T_{qph} \) represents a relaxation time constant attributed to phonon anharmonicity. In this time region, Eq. (4) becomes

\[
\check{D}_q^R(\tau, 0) = -i e^{-i\omega \tau} \xi_q(\tau, 0) V_{qph, ph}^{L\dagger}(0) \delta(\tau),
\]

(9)

where the relations of \( V_{qph, ph}^{R\dagger}(\infty) = \delta_{ph,j} \), \( V_{qph, ph}^{L\dagger}(\tau) \approx 1, [c_q(-\infty), c_q^\dagger(-\infty)] = 1, \) and \( [c_q, D_q^\dagger] = [c_q, A_q^0(kb\dot{b})] = 0 \) are used. In fact, \( \xi_q(\tau, 0) \) given by

\[
\xi_q(\tau, 0)
\]

\[
\approx \exp \left[ -\int_{-\infty}^\tau dt'' \Im E_{qph}(t'') - \int_0^\tau dt'' \Re E_{qph}(t'') - \omega_q \right]
\]

(10)

is approximately unity. Thus, \( \theta_q \) and \( A_q^0 \) are provided as

\[
\theta_q = \frac{\pi}{2} - \arg[\delta V_{qph}],
\]

(11)

modulus \( \pi \), and

\[
A_q^0 = |\delta V_{qph}|,
\]

(12)

respectively, where

\[
\delta V_{qph} = V_{qph, ph}^{L\dagger}(0) - 1.
\]

(13)

Numerical calculations for undoped Si are conducted. Material parameters employed here are given in Ref. 22 with \( \tau_L = 10 \) fs, \( T_q = 66 \) fs equivalent to \( \omega_q = 63 \) meV = 15.2 THz, and \( T_{qph} = 2 \) ps.

### III. EXPERIMENTS

The anisotropic transient reflectivity of \( n \)-doped (\( \sim 1 \times 10^{15} \text{cm}^{-3} \)) Si(001) sample is measured in air at 295 K by the electro-optic (EO) sampling technique.\(^{38}\) Nearly collinear, pump and probe beams — with center frequency \( \omega_p = 2.989 - 3.180 \text{ eV} \) (390 - 415 nm) — are overlapped at a \( 7.2 \times 10^{-7} \text{cm}^2 \) spot on the sample. The maximum average pump power of 18 mW generates \( \Delta \approx 3.0 \times 10^{10} \text{cm}^{-3} \) carriers estimated from the absorption coefficient \( \alpha = 8.0 \times 10^3 \text{cm}^{-1} \) at 397 nm. This is 10 times less than the critical density for screening of the carrier-phonon interaction.\(^{38}\) After reflecting from the sample, the probe is analyzed into polarization components parallel and perpendicular to that of the pump and each is detected with a photodiode. The resulting photocurrents are subtracted and their difference \( (\Delta R_{\parallel} - \Delta R_{\perp})/R \) was recorded versus the pump-probe delay. The delay is scanned over \( 8 \) ps at 20 Hz frequency.\(^{22}\)

### IV. RESULTS AND DISCUSSION

Figure 11 shows the calculated results of \( Q_q(\tau) \) as a function of \( \tau \) and the associated \( S_q(\omega) \) for \( \Delta = -136 \) meV, \( -54.4 \) meV, \(-27.2 \) meV, and 108.8 meV, respectively with \( \Omega_{qph} = 108.8 \) meV. Here, \( \Delta \) represents the detuning defined as the difference of the center frequency of a pump-laser pulse \( \omega_p \) from the direct band gap energy at \( \Gamma \) point \( E_g \), that is, \( \Delta = \omega_p - E_g \). \( Q_q(\tau) \) in Fig. 11(c) looks almost sinusoidal. The spectrum \( S_q(\omega) \) in Fig. 11(c) peaks at \( \omega = \omega_q \) with a symmetric profile. It is seen that
in Figs. 1(b) and 1(c), the amplitudes of $Q_\tau(\tau)$ in the ETR ($\tau \lesssim 100$ fs) are much larger than those in the classical region ($\tau \gtrsim 100$ fs), and the spectral profiles are found asymmetric in $S_\omega(\omega)$ seen in Fig. 1(f) and 1(g). In contrast, in Fig. 1(d), $Q_\tau(\tau)$ oscillates almost in a sinusoidal manner with a constant amplitude to show a symmetric spectral profile as seen in Fig. 1(h). The irregularity with the enhancement of amplitudes in the ETR shown in Figs. 1(b) and 1(c) is attributed to the almost energetically resonant interaction between both modes of plasmon and LO-phonon, as discussed in Ref. 23, so is the associated spectral asymmetry.

The asymmetry observed in $S_\omega(\omega)$ of Fig. 1 is evaluated by fitting these spectra in the vicinity of each peak to Fano’s spectral formula:

$$I(\omega) = C\frac{(q_\omega + \varepsilon)^2}{1 + \varepsilon^2} + \text{const.},$$

where $\varepsilon = (\omega - \omega_c - \Delta\omega) / \Gamma$, $C$ is the amplitude, $q_\omega$ is the asymmetry parameter, $\omega_c$ is the unperturbed frequency, and the frequency shift $\Delta\omega$ and the broadening parameter $\Gamma$ are the carrier density dependent real and imaginary parts of the LO phonon self-energy associated with the interaction with photogenerated carriers. Figure 2 shows the inverse of the asymmetry parameter $1/q_\omega$ having a negative value as a function of $\Delta$ with $\Omega_{\text{exc}} = 108.8$ meV; where a spectrum $S_\omega(\omega)$ becomes symmetric with the decrease of $1/q_\omega$, while this becomes asymmetric with the increase of it aside from $1/q_\omega \gg 1$ showing a (symmetric) spectral dip. At $\Delta < -100$ meV, $1/q_\omega$ is reduced. As $\Delta$ increases, $1/q_\omega$ becomes larger, because the plasmon-phonon resonance likely occurs in the ETR. Within our calculations, the profile is the most asymmetric at $\Delta = -54.4$ meV with $1/q_\omega = -0.286$. As $\Delta$ further increases, $1/q_\omega$ approaches zero again to show symmetric profiles.

Figure 3(a) shows the experimental results of transient EO reflectivity as a function of time delay for different photon energy $\omega_p$, and the FTs of these oscillatory signals are shown in Fig. 3(b). For the 2.989 eV excitation, aperiodic electronic response near the zero delay dominates the signal. For higher energies, in addition, there appears a coherent oscillation with a period of $\sim 66$ fs that persists for $\sim 8$ ps due to the $|q| \approx 0$ coherent LO phonons. The phonon amplitude monotonically increases with increasing the photon energy, reaching a maximum of $\Delta R_{\text{eo}}/R \sim 2.5 \times 10^{-5}$ at the high-energy limit of the tuning range, where it is comparable to the electronic response. With the spontaneous Raman spectra, the LO phonon signal is enhanced by resonance with the direct band gap of Si (attributed to two nearly overlapping transitions $E'_0$ (3.320 eV) at the $\Gamma$ point and the more intense $E_1$ (3.396 eV) for a range of momenta along $\Lambda^{13}$). The FT spectra show a pronounced asymmetry, which we fit to a Fano lineshape given by Eq. (14).22

Further, Fig. 3(c) shows the inverse of the asymmetry parameter $1/q_\omega$ as a function of $\omega_p$, which is extracted from the signals of Fig 3(b) in the same manner as that of Fig 2. The intensity of the pulse laser irradiated here corresponds to $\Omega_{\text{exc}} = 110$ meV almost equal to that used in the theoretical calculations for Figs. 1 and 2. In actual experiments accompanying high-density carrier excitation, a primitive bandgap $E_g \approx 3.3$ meV is likely modified to $E_g$ due to the effect of bandgap renormalization.2 Accordingly, it is considered that the photon energy $\omega_p$
necessary for the carrier excitation is reduced to some extent from \( \omega_0 \), that is, \( \omega_p = \omega_0 - \Delta_g \) with the magnitude of the bandgap renormalization as \( \Delta_g \equiv E_g - E_g \). Thus, the detuning is represented by \( \Delta = \omega_p - E_g \). As shown in Figs. 2(b) and 2(c), for \( \omega_p \lesssim 3.05 \text{ eV} \), the spectral profiles are asymmetric, and the profile is the most asymmetric at \( \omega_p = 3.025 \text{ eV} \) with \( 1/q_a = -0.348 \), where the amplitudes of the time signals in the ETR are much larger than those in the classical region. On the other hand, for \( \omega_p \gtrsim 3.05 \text{ eV} \), as \( \omega_p \) increases, the profile becomes symmetric. These results are in agreement with the calculated results shown in Figs. 1 and 2 if the estimate of \( \Delta_g \) is considered to be roughly 200 meV. Actually, the photoexcited carrier density is \( 2.0 \times 10^{19} \text{ cm}^{-3} \) for \( \Delta = 54.4 \text{ meV} \) in the present calculations, leading to \( \omega_0 \approx 3.35 \text{ eV} \). On the other hand, the photoexcited carrier density is \( 3.0 \times 10^{19} \text{ cm}^{-3} \) for \( \omega_p = 3.12 \text{ meV} \) in the experiment cited in Ref. 8. Because both of the photoexcited carrier densities are almost equal, we obtain \( \Delta_g \approx 230 \text{ meV} \), which is the same order of magnitude as that calculated by a first-principle technique and the GW approximation for the self-energy operator.  

Next, with the goal of deepening the understanding of the asymmetry observed in Fig. 2, first, we examine the detail of the pronounced behavior of the CP signals shown in Figs. 1(b) and 1(c) in the time region of \( \tau \lesssim 20 \text{ fs} \) much smaller than the period \( T_q \). Figure 1 shows the real parts of adiabatic energy curves of plasmon mode \( E_{qpl}(\tau) \) with respect to \( \tau \) for \( \Delta = -54.4 \) and -27.2 meV with \( \Omega_{0cv} = 108.8 \text{ meV} \). \( E_{qpl}(\tau) \)'s are renormalized by the electron-laser interaction, the Hartree-Fock interaction, and the electron-LO-phonon interaction to lead to the deviation from an unrenormalized plasmon frequency \( \omega_{qpl}(\tau) \) to some extent. In particular, this stands out in the region of \( \tau \lesssim 10 \text{ fs} \). Actually, at \( \tau = 9 \text{ fs} \), despite \( \tau > \tau_L/2 \), \( \text{Re}[E_{qpl}(\tau)] \) 's differ from \( \omega_{qpl}(\tau) \) by roughly 10 and 5 meV for \( \Delta = -54.4 \) and -27.2 meV, respectively, due to the renormalization of still non-negligible electron-laser interaction in the tail region of the pulse, where \( \Omega_{cv}(\tau) = 11.5 \text{ meV} \). As time passes, \( \Omega_{cv}(\tau) \) vanishes, and \( \text{Re}[E_{qpl}(\tau)] \) becomes closer to \( \omega_{qpl}(\tau) \) aside from the energy difference between these two energy-values due to the Hartree-Fock interaction and the electron-LO-phonon interaction that are still retained in the ETR, as seen in Fig. 1.

Concerning another adiabatic energy of LO-phonon mode \( E_{qph}(\tau) \), the real part of it, \( \text{Re}[E_{qph}(\tau)] \), is almost equal to \( \omega_q \) within a couple of meV due to the renormalization of the electron-LO-phonon interaction, thus, for the sake of simplicity, hereafter, let \( E_{qph}(\tau) \) be represented by \( \omega_q \) in Fig. 3. The way of interaction between the plasmon and LO-phonon modes can be understood in terms of the following two-state models in the adiabatic picture as the LZ model and the RZ model. In the LZ model, two adiabatic-energy curves tend to swerve sharply around the local time \( \tau = \tau_{LZ} \), at which both are closest to each other forming anti-crossing, while in the RZ model, these curves evolve in a parallel manner over time \( \tau \) after \( \tau_{RZ} \) with almost energetically degenerate. It is seen in Fig. 3 that for \( \Delta = -27.2 \text{ meV} \), \( \text{Re}[E_{qpl}(\tau)] \) traverses \( \text{Re}[E_{qph}(\tau)] \) around \( \tau_{LZ} = 9 \text{ fs} \), while for \( \Delta = -27.2 \) and -54.4 meV, \( \text{Re}[E_{qph}(\tau)] \) becomes constant after \( \tau_{RZ} = 12 \text{ fs} \) to form the RZ coupling in the ETR. Let the energy difference of \( \text{Re}[E_{qpl}(\tau)] \) from \( \text{Re}[E_{qph}(\tau)] \) in the ETR be represented by \( \delta E_q \), that is, \( \delta E_q \equiv \text{Re}[E_{qpl}(\tau)] - \text{Re}[E_{qph}(\tau)] \); where \( \delta E_q \) is considered almost constant in \( \tau > \tau_{RZ} \). It is evident that with the decrease of \( \delta E_q \), the effect of the RZ coupling becomes more significant. Actually, \( \delta q \) in Fig. 3 is put in an increasing order of \( \delta E_q \) as -54.4, -27.2, -136.0, and 108.8 meV. Incidentally, for \( \Delta = 108.8 \text{ meV} \), an anti-crossing due to the LZ coupling likely occurs just in the region of \( \tau \lesssim \tau_L/2 \), though the overall oscillatory pattern is little affected by this.

The interaction between the two modes of plasmon and LO-phonon causes abrupt changes of \( A_p(\tau) \) and \( \Theta_q(\tau) \) in the oscillatory pattern of \( Q_{q}(\tau) \). Figure 3 is the enlarged view of Figs. 1(b) and 1(c) in the lim-
FIG. 4. The real part of the adiabatic eigenvalue of the plasmon mode $\text{Re}[E_{q \text{pl}}(\tau)]$ (in the unit of meV) as a function of $\tau$ (in the unit of fs) for $\Delta = -54.4$ meV (blue square) and -27.2 meV (green square). The blue and green dot lines represent the associated plasma frequencies $\omega_{q \text{pl}}(\tau)$, and the black dash line represents the bare phonon energy $\omega_q$.

FIG. 5. The enlarged view of Figs. 1(b) and 1(c) in the limited temporal region of $\tau$ for $\Delta = (a) -54.4$ meV and (b) -27.2 meV, respectively.

FIG. 6. The enlarged view of Fig. 3(a) in the limited temporal region for $\omega_p = (a) 3.025$ eV and (b) 3.040 eV.
in Fig. 1. Hence, $S_q(\omega)$ proves asymmetric if $S_q^{(\text{in})}(\omega)$ is comparable to or dominant over $S_q^{(\text{out})}(\omega)$; otherwise this is symmetric. The asymmetric spectra of Figs. 1(f) and 1(g) are the case. It is noted that the anomaly arising from the LZ coupling shown in Fig. 1(b) is less effective against $S_q^{(\text{in})}(\omega)$ than the contribution from the RZ coupling, since the former coupling is localized just in vicinity of $\tau_{LZ}$. To be more specific, the degree of asymmetry in $S_q(\omega)$ is mostly governed by the magnitude of the RZ coupling in the ETR that is evaluated in terms of $\delta E_q$. Actually, with the increase in $\delta E_q$, $S_q(\omega)$ is apt to be more symmetric within the scope of the calculations implemented here, as is shown in Figs. 2 and 3(c).

Incidentally, $\delta E_q$ is determined by the Rabi frequency $\Omega_{q\text{ev}}$ as well as $\Delta$, because $\text{Re}[E_{q\text{ph}}(\tau)]$ as well as $\omega_{q\text{ph}}$ is subject to the photoexcited carrier density.

Below, we give consideration to the alteration pattern of $1/q_a$ when a pulse area represented by $S_L$ exceeds $\pi$, that is, $S_L/\pi > 1$; this pulse is termed as pulse 1 hereafter. For the sake of simplicity, $S_L$ is assumed to be evaluated as the product of the nutation frequency given by

$$\Omega_N = \sqrt{\Omega_{q\text{ev}}^2 + \Delta^2}$$

and $\tau_L$, that is, $S_L = \Omega_N \tau_L$, where a dispersionless two-level model is adopted without the Coulomb correction to $\Omega_{q\text{ev}}$. When the pump-pulse irradiation is completed, the total amount of photoexcited carrier density per site, denoted as $D_L$, is given by

$$D_L = \left(\frac{\Omega_{q\text{ev}}}{\Omega_N}\right)^2 \sin^2\left(\frac{S_L}{2}\right).$$

This expression is obtained by employing a square pulse with $f(t) = \theta(t + \tau_L/2)\theta(\tau_L/2 - t)$ in Eq. 1 instead of the Gaussian pulse adopted above. Another pulse termed as pulse 0 with pulse area $S_L^0 < \pi$ is introduced, where this pulse has a nutation frequency $\Omega_N^0$ with $\Omega_{q\text{ev}}^0$ and $\Delta^0$ as Rabi frequency and detuning, respectively; $\Omega_N^0 = \sqrt{(\Omega_{q\text{ev}}^0)^2 + (\Delta^0)^2}$. Let the special case of $\Omega_{q\text{ev}}^0 = 108.8$ meV and $\Delta^0 = -54.4$ meV — providing $\Omega_N^0 = 121.6$ meV and $S_L^0/\pi = 0.5880 < 1$ — be taken into consideration, where the obtained asymmetry parameter is represented as $1/q_a^0 \equiv -0.286$. If the two pulses 0 and 1 generate the same carrier density of $D_L$, the condition of $\delta E_q \approx 0$ is realized in both cases, leading to the maximized RZ coupling. This condition is met by taking, for instance, $\Omega_N = 255.8$ meV with $\Omega_{q\text{ev}} = 244.8$ meV and $\Delta = -74.17$ meV, which leads to $S_L/\pi = 1.3766 > 1$.

Now, the degree of spectral asymmetry $1/q_a$ of the CP generated by pulse 1 is examined. To this end, we consider the alteration of $\theta_q$ and $A_q^0$ as a function of $\Delta$, as shown in Fig. 4 for different values of $\Omega_{q\text{ev}}$‘s of 54.4, 108.8, and 244.8 meV. $\theta_q$ and $A_q^0$ are determined by $\delta V_{q\text{ph}}$, as seen in Eqs. (11)–(13): $\delta V_{q\text{ph}}$ is subject to the photoexcited carrier density, similarly to $\delta E_q$. Thus, with the increase of the carrier density, $(\pi/2 - \theta_q)$ and $A_q^0$ tend to increase as a whole in Figs. 7(a) and 7(b), respectively, aside from the non-monotonic change of $A_q^0$ for $\Omega_{q\text{ev}} = 244.8$ meV due to the optical mutation.

The four values arrowed in Fig. 4 represent $\theta_q$ and $A_q^0$ for $(\Omega_{q\text{ev}}, \Delta) = (244.8\text{meV}, -74.17\text{meV})$ and $(\Omega_{q\text{ev}}, \Delta) = (108.8\text{meV}, -54.4\text{meV})$. Although the RZ coupling is caused in a similar way for both sets of $(\Omega_{q\text{ev}}, \Delta)$, the resulting $A_q^0$‘s are different roughly by three times; $\theta_q$‘s are almost identical to each other presumably by accident, which equal approximately $80^\circ$. This difference arises from the fact that $A_q^0$ and $\theta_q$ are determined through $V_{LZ,\text{ph},\text{ph}}(0)$ by $\Omega_{q\text{ev}}(0)$ as well as the photoexcited carrier density, whereas the RZ coupling is determined solely by the latter. Therefore, the resulting $1/q_a$-values are not identical in these two $(\Omega_{q\text{ev}}, \Delta)$‘s of concern, namely, $1/q_a = 1/q_a^0$, since the degrees of contribution of $S_q^{(\text{out})}(\omega)$ to $S_q(\omega)$ are different in these two cases. However, it is possible that the value of $1/q_a^0$ is retrieved by adjusting the value of $\Omega_N$ so that the condition $S_q^{(\text{out})} \ll S_q^{(\text{in})}$ is ensured. Actually, the set of $(\Omega_{q\text{ev}}, \Delta) = (313.1\text{meV}, -42.78\text{meV})$ — with $\Omega_N = 316.0$ meV and $S_L/\pi = 1.5$ — provides the same value of $\delta E_q$ as that for $(\Omega_{q\text{ev}}, \Delta) = (\Omega_{q\text{ev}}^0, \Delta^0)$ and the value of $A_q^0$ smaller than that for $(\Omega_{q\text{ev}}, \Delta) = (244.8\text{meV}, -74.17\text{meV})$, though not shown here. In any case, it would be stated that the spectral asymmetry given by $1/q_a$ varies more or less following the optical

![FIG. 7. The calculated results of (a) $\theta_q$ and (b) $A_q^0$ as a function of $\Delta$ (in the unit of meV) for $\Omega_{q\text{ev}} = 54.4$ meV (blue diamond), 108.8 meV (red square), and 244.8 meV (orange triangle)]. As regards the four arrowed values, consult the text for detail.](image-url)
Finally, two more remarks are given regarding the spectral asymmetry of concern. First, it is pointed out that the spectral asymmetry attributed to the CP generation is observed exclusively in a lightly $n$-doped Si crystal and semimetals/metals such as Bi and Zn,

\[ \delta E \]

though not observed in a GaAs crystal.\cite{13,14,45,46} Obviously, the amplitude $|Q_q(\tau)|$ in the classical region for GaAs is much greater than that for Si, because in the former, the CP is driven by a much stronger electron-LO-phonon coupling due to the Fröhlich interaction. Therefore, it is speculated that $S_q^{\text{out}}(\omega)$ dominates $S_q(\omega)$ to result in symmetric spectral-profile, that is, $S_q^{\text{out}}(\omega) \gg S_q^{\text{in}}(\omega)$. However, it might be possible that $S_q(\omega)$ is asymmetric when a certain condition leading to $\delta E_q \approx 0$ is ensured. Thus, it would also be necessary to scrutinize spectral profiles at time $\tau$ in the ETR under this condition, for instance, by using the continuous-wavelet transform of $Q_q(\tau)$.

Second, it is reported that an asymmetric spectral-profile observed in a lightly $n$-doped Si crystal is attributed to transient Fano resonance.\cite{2,22,32} In Ref. 22, based on the PQ model incorporating the Fano model,\cite{21} the spectral asymmetry attributed to the Fano resonance is obtained just in the ETR, where $Q_{\text{env}} = 16.4$ meV and $\Delta = 82$ meV corresponding to $\delta E_q \approx -40$ meV; hence, the RZ model is no longer significant. There, $S_q(\omega)$ also shows the asymmetry, since the associated $Q_q(\tau)$ tends to vanish rapidly out of the ETR, and thus $S_q^{\text{in}}(\omega)$ becomes dominant over $S_q^{\text{out}}(\omega)$. Therefore, it is speculated that the asymmetry parameter $1/\sqrt{q_0}$, discussed in Figs. 2 and 3(c) becomes finite, namely, non-zero, due to the Fano resonance, even though $|\delta E_q|$ increases considerably with $\delta E_q < 0$.

V. CONCLUSIONS

The degree of asymmetry of the spectral profiles of the CP time signals is scrutinized in undoped Si by using the PQ model, and the adiabatic energy curves of the plasmon and the LO-phonon are examined based on the LZ and RZ models. The asymmetric spectral-profiles are discerned, as long as the RZ interaction is dominant in the ETR with $S_q^{\text{in}}(\omega)$ greater than or comparable with $S_q^{\text{out}}(\omega)$. Since the magnitude of the RZ interaction depends decisively on the adiabatic plasmon energy, thus the degree of asymmetry varies with respect to the photoexcited carrier density. Actually, it is confirmed in both of the present calculation and experiment that the spectra become more symmetric with larger change of the carrier density from the critical carrier density at which the effect of the RZ interaction is maximized.

The particular emphasis is put on the degree of this asymmetry in both of the far-lower carrier density region ($\omega_{\text{qpl}} \ll \omega_q$) and far-higher carrier density region ($\omega_{\text{qpl}} \gg \omega_q$) than the region concerned in this study ($\omega_{\text{qpl}} \approx \omega_q$). In the lower carrier density region, it is reported that the transient Fano resonance with an asymmetric profile is discerned in the ETR\cite{22} this is caused by the interaction between the LO-phonon mode and the single-particle excitation mode, and there is little contribution from the plasmon mode. On the other hand, in the higher carrier density region where pulse areas of the corresponding irradiated laser pulses exceed $\pi$, it would be possible that the degree of asymmetry of the profile varies following the optical rotation of the photoexcited carrier density. Here, the RZ interaction between the LO-phonon mode and the plasmon mode in the ETR still plays a significant role of determining the degree of asymmetry. These two phenomena occurring in the regions of $\omega_{\text{qpl}} \ll \omega_q$ and $\omega_{\text{qpl}} \gg \omega_q$ are still unexplored in experiments. Therefore, it is expected to measure the spectral profiles of CP over the wider region of photoexcited carrier density than the present, and to reveal the underlying quantum-mechanical effects governing the alteration of the profiles.

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