Research Article

Improving Dam Seepage Prediction Using Back-Propagation Neural Network and Genetic Algorithm

Xuan Zhang, Xudong Chen, and Junjie Li

School of Water Conservancy Science and Engineering, Zhengzhou University, Zhengzhou 450001, China

Correspondence should be addressed to Xudong Chen; chenxudong@zzu.edu.cn

Received 20 September 2019; Revised 16 December 2019; Accepted 7 January 2020; Published 13 April 2020

Copyright © 2020 Xuan Zhang et al. This is an open access article distributed under the Creative Commons Attribution License, which permits unrestricted use, distribution, and reproduction in any medium, provided the original work is properly cited.

Statistical model is a traditional safety diagnostic model for dam seepage. It can hardly display the nonlinear relationship between dam seepage and the load sets and has the disadvantage of poor extension prediction. In this paper, the theories of Back Propagation Neural Network (BPNN) combined with Genetic Algorithm (GA) are applied to the seepage prediction model. Taking a typical dam in China as an example, the prediction results of BPNN-GA model and statistical model are compared with the monitoring values. The results show that the improved dam seepage model enhances the ability of nonlinear mapping and generalization and makes the seepage prediction more accurate and reasonable in the near future. According to the established criterion, the safety state of the dam in flood season is evaluated.

1. Introduction

Seepage can directly reflect the dam working state and plays an important role in the dam safety monitoring. Related statistical studies have shown that dam break caused by seepage accounts for 30%–40% of the total dam break [1]. Therefore, developing or improving a reliable model, timely analyzing the dam seepage monitoring data, and predicting its change trend are of great significance to grasp the safety state of dam seepage.

Fanelli from Italy and Roeha from Portugal first applied the statistical regression method to the field of dam safety monitoring. Afterwards, Fanarin and others combined the theory of finite element with the monitoring data-derived deterministic model and hybrid model [2]. In recent years, with the continuous development of numerical simulation technology, scholars have introduced different prediction methods into the study of dam seepage analysis models [3–9]. Artificial Neural Network (ANN) is a research hotspot in the field of artificial intelligence since the 1980s. For the water conservancy project, ANN is a new and very important frontier research topic, and they have mature applications in many aspects including hydrological simulating, flood predicting, safety monitoring, and comprehensive evaluating [10–19]. Dawson et al. [10] used the Radial Basis Function Neural Network (RBFNN) to simulate the local rainfall-runoff evolution of the Yangtze River in China, which promoted its development in the field of hydrological simulation. Campolo et al. [11] established a flood forecasting model based on the ANN and used real-time information of a watershed to predict the water level evolution. Jeong et al. [12] used the ANN method to establish the rainfall-runoff model in order to predict the ensemble streamflow. Wang et al. [13] used the improved ANN to predict the displacement of a concrete-faced rockfill dam, which provided a new idea for monitoring dam displacement. Mata [14] combined the ANN model with the comprehensive evaluation system and proposed the corresponding method for evaluating the dam working behaviour. Zadhesh et al. [15] adopted the ANN to estimate the secondary permeability required for the grouting quality assessment on the Cheraghvays dam’s foundation. Unes et al. [16] used the ANN to predict daily reservoir levels of the Millers Ferry Dam on the Alabama River in the USA. Li et al. [17] applied the Back Propagation Neural Network (BPNN) to analyze the relationship between the sediment-flushing efficiency of the Three Gorges Reservoir and its influencing factors. Shaw et al. [18] successfully simulated the prediction ability of a high-fidelity hydrodynamic and water quality model using the ANN. Bui et al. [19] proposed a novel hybrid artificial intelligent approach for modeling and
2 Mathematical Problems in Engineering

2. Dam Seepage Statistical Model

Dam seepage monitoring variables are generally divided into two categories: uplift pressure and leakage. Taking the uplift pressure as an example, it is mainly affected by factors including water pressure, temperature, and time-effect [2, 20–25], which can be shown as

\[ \delta = \delta_H + \delta_T + \delta_\theta, \]

where \( \delta \) is the uplift pressure, \( \delta_H \) is the water pressure component, \( \delta_T \) is the temperature component, and \( \delta_\theta \) is the time-effect component.

(1) Water Pressure Component \( \delta_H \). The change of reservoir water levels has a great influence on the seepage of the dam and has a certain delay [2]. The equivalent water level can be calculated according to the method in the literature [21–23] to express the delay effect of seepage. \( \delta_H \) has a linear relationship with water level, so the water pressure component can be expressed as

\[ \delta_H = a_1 H^1, \]

where \( H^1 \) is the equivalent water level on the monitoring day and \( a_1 \) is the regression coefficient.

(2) Temperature Component \( \delta_T \). The temperature component refers to the seepage change caused by the temperature change of the dam concrete and foundation rock. Thermal expansion reduces cracks, enhances impermeability, and then slows down seepage. Cooling shrinkage increases cracks, reduces impermeability, and thus intensifies seepage. The temperature of the dam body and foundation rock varies periodically with atmospheric temperature, which can be expressed with a periodic function. Considering the linear relationship between seepage and temperature, the multiperiod harmonic is chosen as the factor to represent the temperature component:

\[ \delta_T = \sum_{i=1}^{\frac{\pi}{2}} \left[ b_{1i} \sin \frac{2\pi it}{365} + b_{2i} \cos \frac{2\pi it}{365} \right], \]

where \( t \) is the number of days from the initial monitoring day to the monitoring day and \( b \) is the regression coefficient.

(3) Time-Effect Component \( \delta_\theta \). The time-effect component is an irreversible component that develops in a certain direction over time. It mainly reflects the influence of dam body material creep, dam foundation rock creep, rock mass joint crack, and weak structure on uplift pressure. Its mechanism is complicated, and the accurate expression is often difficult to derive [23]. Typically, the variation of the time-effect component usually changes sharply at the beginning and gradually turns stable during the later period. The general variation law of the time-effect component can be expressed by the combination of two empirical formulas, which can be expressed as

\[ \delta_\theta = c_1 \theta + c_2 \ln \theta, \]

where \( \theta = 0.01 t \) and \( c \) is the regression coefficient.

In summary, the statistical model of the uplift pressure can be expressed as

\[ \delta = \sum_{i=0}^{\infty} a_i H^i + \sum_{i=1}^{\infty} \left[ b_{1i} \sin \frac{2\pi it}{365} + b_{2i} \cos \frac{2\pi it}{365} \right] + c_1 \theta + c_2 \ln \theta. \]

3. Improved Dam Seepage Model Based on BPNN and GA

3.1. Back-Propagation Neural Network. The Back Propagation Neural Network (BPNN) was proposed by Rumelhart and McClelland in 1986. It is a multilayer feedforward network trained by the backpropagation algorithm and is also the most widely used neural network model at present. The BPNN consists of input layer, hidden layer, and output layer, and each layer contains several neurons [26]. The neurons in the same layer are not connected with each other, while the neurons in the adjacent layers are connected with each other, as shown in Figure 1.

Assuming the number of samples \((x_i, y_i) (i = 1, 2, ..., n)\) is \( n \), the \( i \) is one of the samples, \( x_i \) is the input vector, and \( y_i \) is the expected output vector of the BPNN. Taking the node \( j \) at the \( m \)-level as the research object, when sample \( i \) is input, the node \( j \) receives the output information of the previous layer as follows:

\[ I_{ji}^m = \sum_{k=1}^{n_i} \omega_{kj} \cdot O_{ki}^{m-1}, \]

where \( k \) is a node in the upper layer, \( n_i \) is the number of nodes in this layer, \( \omega_{kj} \) is the connection weight between the node \( k \) and the node \( j \), and \( O_{ki} \) is the output signal of the node \( k \).

The output value of the node \( j \) after the action function can be expressed as

\[ O_{ij}^m = f(I_{ji}^m), \]

where \( f(x) \) is the function at the node \( j \). The sigmoid function is often used in practical applications. The output
value of the sigmoid function is between (0, 1). The form of the function is as follows:

$$f(x) = \frac{1}{1 + e^{-x}}.$$  \hspace{1cm} (8)

According to equations (6)–(8), the output value \( \hat{y}_i \) of the output layer can be obtained by calculating the output layer by layer.

In the process of error backpropagation, it is necessary to define an objective function. That is, the sum of squares of errors between the output value \( \hat{y}_{ji} \) of the output layer and the expected output value \( y_{ji} \)

$$E_i = \frac{1}{2} \sum_{j=1}^{l} (y_{ji} - \hat{y}_{ji})^2,$$  \hspace{1cm} (9)

where \( l \) is the number of nodes in the output layer of the BPNN. In practical applications, there is often only one node in the output layer, so the above expression can be expressed as

$$E_i = \frac{1}{2} (y_i - \hat{y}_i)^2.$$  \hspace{1cm} (10)

Then, the total error is

$$E = \frac{1}{2n} \sum_{i=1}^{n} E_i,$$  \hspace{1cm} (11)

where \( n \) is the number of samples.

The process of error adjustment is equivalent to an unconstrained optimization problem, that is, to minimize \( E \) by adjusting the connection weights without any restriction:

$$E(\omega) = \min.$$  \hspace{1cm} (12)

Repeat the above steps and constantly correct the weights of BPNN until the error meets the requirement.

BPNN, due to its ability to map complex nonlinear and unknown relationships, is a preferred choice among researchers for modeling unstructured problems and has been well applied in many practical engineering problems. However, it also has some shortcomings, such as being affected by the initial values and easily falling into a local extremum [26–28]. In this paper, the Genetic Algorithm (GA) is used to optimize the initial weights and thresholds of the BPNN, so as to improve the convergence speed of the BPNN and reduce the possibility of the BPNN algorithm falling into the local extremum.

3.2. Optimizing BPNN by Genetic Algorithm. Genetic Algorithm (GA) is a gradient-free global optimization and search technique inspired by the evolutionary processes namely, natural selection and genetic variation. It was first proposed by Professor Holland of the United States in the 1970s. It operates directly on the structural object without restriction of derivation and function continuity. It adopts the probabilistic optimization method, which can automatically obtain and guide the optimization search space, adjust the search direction adaptively, and does not need to determine the rule. Different from the traditional optimization algorithm, the GA allows simultaneous search for optimal solutions in different directions, instead of starting from one direction [26]. GA has no specific requirements for the state of the objective function, and it has a good global search ability. Therefore, GA can be used to optimize the connection weights and thresholds of the BPNN [26–29], and the flow chart is shown in Figure 2.

BPNN is based on gradient descent algorithm for training and weight adjustment. Before training, the BPNN randomly initializes the connection weights and threshold of each layer to the values between interval [0, 1]. This method of random initialization tends to slow down the convergence speed of the BPNN and lead to local extremum problem, while GA has strong global convergence, but the ability of local refinement is deficient. So, we can combine GA with BPNN. When the convergence speed of BPNN is slow, the connection weights and threshold of each layer in the network can be used as the input information of GA. Through the genetic operator, the optimal individual is obtained. The optimal individual obtained by GA is decoded and assigned as the initial weights and thresholds of BPNN. Then, BPNN is used for local optimization, and the output values with global optimal solution are obtained.

From the point of view of BPNN based on GA, the method is to use GA to search the solution space of target information. Then, when the GA finds a better network form, it uses the BP algorithm to locate so as to find the optimal solution of the problem. The specific steps are as follows [30–32]:

1. **Initial Population.** Firstly, the topological structure of the BPNN should be determined, and then the length of individual should be determined according to the network structure. All weights and thresholds in the network are real coded as a set of chromosomes \( X \):

$$X = [\omega_{11}, \omega_{12}, \ldots, \omega_{mn}, \theta_1, \theta_2, \ldots, \theta_m, \varphi_{11}, \varphi_{12}, \ldots, \varphi_{mn}, \mu_1, \mu_2, \ldots, \mu_l].$$  \hspace{1cm} (13)

where \( \omega \) is the weight between the input layer and the hidden layer, \( \theta \) is the connection threshold between each layer of the hidden layer, \( \varphi \) is the weight between the hidden layer and the output layer, and \( \mu \) is the output layer threshold.

2. **Fitness Function.** The reciprocal of the sum of the absolute errors between the predicted output and the
Determine the structure of BPNN

Code

Initialize population

Calculate fitness

Whether the fitness meets the requirements?

N

Select

Cross

Vary

Output result

Adjust weights

Y

Decode

Figure 2: Flow chart of BPNN-GA.

The expected output of the BPNN is taken as the fitness function \( F \):

\[
F = \frac{1}{\sum_{i=1}^{N} \sum_{j=1}^{m} (y_j^i - o_j^i)^2}
\]

where \( N \) is the number of training samples, \( m \) is the dimension of the output variables, \( y_j^i \) is the target value of the output node \( j \) of the BPNN when sample \( i \) acts, and \( o_j^i \) is the output value.

(3) Genetic Operations.

(1) Selection. Using the roulette method to select the operator, the probability of being selected is

\[
P_i = \frac{F_i}{\sum_{i=1}^{c} F_i}
\]

where \( y_{jk} = y_{jk}^r + y_{jk}(1-r), \)

\[
y_{jk} = y_{jk}^r + y_{jk}(1-r),
\]

\[
y_{ij} = \begin{cases} y_{ij}^r + (y_{ij} - y_{max})r_1 \left( 1 - \frac{s}{s_{max}} \right), & r_2 \geq 0.5, \\ y_{ij}^r + (y_{min} - y_{ij})r_1 \left( 1 - \frac{s}{s_{max}} \right), & r_2 < 0.5, \end{cases}
\]

where \( c \) is the number of individuals in the population.

(2) Crossover. Using the real number cross method, the cross operation method of the \( i \)th and \( j \)th individual at the position \( k \) is as follows:

where \( y_{ik} \) and \( y_{jk} \) represent, respectively, the gene of the \( i \)th and \( j \)th individual at the position \( k \), and \( r \) is the random number between \((0, 1)\).

(3) Mutation. Selecting the \( j \)th gene of the \( i \)th individual \((y_{ij})\) for mutation operation, the method is as follows:

where \( y_{max} \) is the upper bound of \( y_{ij} \), \( y_{min} \) is the lower, \( s \) is the current number of iterations, \( s_{max} \) is the maximum number of iterations, and \( r_1 \) and \( r_2 \) are the random numbers between \([0, 1]\).

(4) Decode. The weights and thresholds of GA output are taken as the initial weights and thresholds of BPNN. BPNN carries out forward propagation, calculates global error, adjusts network parameters, and repeats learning training.

Using GA to optimize the BPNN has a great probability to avoid the network falling into a local extremum and to speed up the training of the network, and the final connection weights will be more stable.

3.3. Seepage Model Based on BPNN-GA. The research object of this paper is the dam seepage prediction model, so the output variable is the predicted value of uplift pressure of dam foundation in a certain period of time in the future. The prediction model is designed as a three-layer BPNN. Combining the seepage theory with BPNN-GA, in the improved model, the input variables are recorded as \( x \):

\[
x = \left( H^*, \sin \frac{2\pi t}{365}, \cos \frac{2\pi t}{365}, \sin \frac{4\pi t}{365}, \cos \frac{4\pi t}{365}, \theta, \ln \theta \right)
\]

where the meaning of each letter is the same as equation (5).

The output variable is the uplift pressure \( y \), and denote the sample set as \( Q_m \):

\[
Q_m = \{x_1, y_1, x_2, y_2, \ldots, x_m, y_m\},
\]

where \( x_i \) represents the input variables of the \( i \)th group and \( y_i \) represents the corresponding uplift pressure monitoring value.

The GA assigns the optimal initial weights to the BPNN through copying, crossing, and varying. The BPNN uses the training set sample \( Q_m \) for machine learning, and the network continuously adjusts the weights to achieve the set minimum error, so that the optimized BPNN can better predict the uplift pressure. At this point, if the test factors are input into the trained model, the model prediction value can be obtained.

3.4. Evaluation Criterion of Dam Seepage State. The BPNN-GA model is used to get the prediction value \((\delta')\) of the uplift pressure at a certain time, which can be compared with the monitoring value \((\delta)\) at that time. According to the probability and statistics theory, the probability of \(|\delta - \delta'|\) (the absolute difference between the monitoring value and the prediction value) falling into \((0, 2S)\) is 95.5%, and the
where the left bank gravity dam sections, 3 # of the main dam is divided into six dam sections, of which 1# and 2# are the left bank gravity dam sections, of which 1# and 2# are the left bank gravity dam sections, and 5 # are the overflow dam sections, and 5 # are the overflow dam sections, and 5 # are the overflow dam sections. fK_his is mainly because the BPNN-GA model has stronger nonlinear mapping and generalization ability, which improves the prediction accuracy of the model. The above results show that the BPNN-GA model has better prediction accuracy.

Since the prediction accuracy of BPNN-GA model is higher than that of the statistical model, the prediction values of the BPNN-GA model are used to evaluate the seepage safety state of Cotton Beach dam in flood season. The prediction values of uplift pressure from July 1 to 31, 2008, of the two points are obtained by BPNN-GA. The results of the absolute difference |δ − δ′| values are shown in Figure 5.

From Figure 5, the absolute difference |δ − δ′| values are relatively small and stable on the whole, illustrating the BPNN-GA model has a good prediction effect. However, Figure 5(a) shows a slightly larger fluctuation on July 29. The affecting factors are analysed, especially the water level, which is often considered to be the main factor. The analysis results show that the upstream water level dropped significantly with a range of 0.6 m on that day, which has a certain impact on data analysis. When there are mutation data in the stationary time series, the BPNN-GA model does not capture its impact well, which leads to the above error. The accuracy of the BPNN-GA model is slightly lower in capturing the mutation data, but it can accurately predict the trend of data change. This is enough to meet the engineering application needs.

In general, all of the absolute difference |δ − δ′| values lie in the interval (0, 2S). According to the criteria in Section 3.4, it can be evaluated that the two points are in the normal seepage state, indicating that the seepage control effect of the overflow dam section is good. Accordingly, the same method can be used to predict the seepage state of other points and analyse the seepage control effect of other dam sections, so...
**Figure 3:** Location of seepage monitoring points.

**Figure 4:** The monitoring and prediction value process line of two points.

**Table 1:** Comparison of prediction results of two models (UP9).

| Date (yyy/m/d) | Measured value (m) | Predictive value (m) |
|---------------|-------------------|---------------------|
|               | BPNN-GA           | Statistical model    |
| 2008/7/1      | 96.61             | 96.42               |
| 2008/7/2      | 96.62             | 96.38               |
| 2008/7/3      | 96.67             | 96.37               |
| 2008/7/4      | 96.45             | 96.34               |
| 2008/7/5      | 96.52             | 96.31               |
|               |                   |                     |
| 2008/7/28     | 96.07             | 96.24               |
| 2008/7/29     | 95.57             | 96.14               |
| 2008/7/30     | 95.71             | 96.24               |
| 2008/7/31     | 96.06             | 96.47               |

**Table 2:** Comparison of prediction results of two models (UP11).

| Date (yyy/m/d) | Measured value (m) | Predictive value (m) |
|---------------|-------------------|---------------------|
|               | BPNN-GA           | Statistical model    |
| 2008/7/1      | 113.50            | 112.92              |
| 2008/7/2      | 113.30            | 112.85              |
| 2008/7/3      | 113.26            | 112.83              |
| 2008/7/4      | 113.14            | 112.78              |
| 2008/7/5      | 113.03            | 112.73              |
|               |                   |                     |
| 2008/7/28     | 112.40            | 112.48              |
| 2008/7/29     | 112.02            | 112.30              |
| 2008/7/30     | 112.37            | 112.45              |
| 2008/7/31     | 113.12            | 112.81              |
that the decision-makers can take corresponding counter-
measures in special circumstances.

5. Conclusions

In this paper, the seepage monitoring model of the dam is
studied according to its own working characteristics. Com-
ing the seepage theory with BPNN-GA, an im-
proved seepage model is established and applied to the
monitoring and analysis of the uplift pressure of Cotton
Beach dam. The results are shown as follows:

(1) From the prediction results of the two points,
compared with the statistical model, the BPNN-GA
model has high prediction accuracy and can predict
the trend of data change better. This shows that it is
reasonable and feasible to apply the BPNN and GA
theory to improve the seepage prediction model.

(2) Compared the prediction values of the improved
seepage prediction model with the monitoring
values, according to the established criteria of the
dam seepage safety state, the seepage safety state of
the Cotton Beach dam in flood season is evaluated.
The results show that the seepage state of the two
measuring points are normal, and the seepage
control effect of the overflow dam section is good.
This method can be extended to other points to
obtain a comprehensive seepage safety state and
seepage control treatment effect.

Data Availability

The data used to support the findings of this study are
available from the author upon request.

Conflicts of Interest

The authors declare no conflicts of interest.

Acknowledgments

This research was funded by the National Natural Science
Foundation of China under grant Nos. 51609217 and
51709239.

References

[1] C. Fang and Y. Duan, “Statistical analysis of dam-break in-
cidents and its cautions,” Yangtze River, vol. 41, no. 11,
pp. 96–100, 2010.
[2] Z. Wu, Safety Monitoring Theory & its Application of Hydraulic Structures, Higher Education Press, Beijing, China, 2003.
[3] X. Chen, C. Gu, and H. Chen, "Early warning of dam seepage with cooperation between principal component analysis and least squares wavelet support vector machine," Fresenius Environmental Bulletin, vol. 22, no. 2, pp. 500–507, 2013.
[4] C. Liu, H. Jing, and Y. Cheng, "Application of EMD-ARI model in seepage forecasting of dam," Water Power, vol. 40, no. 7, pp. 49–52, 2014.
[5] K. Roushangar, S. Garekhani, and F. Alizadeh, "Forecasting daily seepage discharge of an earth dam using wavelet-mutual information-Gaussian process regression approaches," Geotechnical and Geological Engineering, vol. 34, no. 5, pp. 1313–1326, 2016.
[6] Y. Xiang, S.-Y. Fu, K. Zhu, H. Yuan, and Z.-Y. Fang, "Seepage safety monitoring model for an earth rock dam under influence of high-impact typhoons based on particle swarm optimization algorithm," Water Science and Engineering, vol. 10, no. 1, pp. 70–77, 2017.
[7] S.-K. Chen, Q.-D. He, and J.-G. Cao, "Seepage simulation of high concrete-faced rockfill dams based on generalized equivalent continuum model," Water Science and Engineering, vol. 11, no. 3, pp. 250–257, 2018.
[8] P. Li, L. Su, and Y. Jia, "BP-RBF neural network seepage model under the influence of various factors," Yellow River, vol. 40, no. 4, pp. 132–135, 2018.
[9] E. Sharghi, V. Nourani, N. Behfar, and G. Tayfur, "Data pre-post processing methods in AI-based modelling of seepage through earthen dams," Measurement, vol. 147, pp. 1–13, 2019.
[10] C. W. Dawson, C. Harpham, R. L. Wilby, and Y. Chen, "Evaluation of artificial neural network techniques for flow forecasting in the river Yangtze, China," Hydrology and Earth System Sciences, vol. 6, no. 4, pp. 619–626, 2002.
[11] M. Campolo, A. Soldati, and P. Andreussi, "Artificial neural network approach to flood forecasting in the river arno," Hydrological Sciences Journal, vol. 48, no. 3, pp. 381–398, 2003.
[12] D.-I. Jeong and Y.-O. Kim, "Rainfall-runoff models using artificial neural networks for ensemble streamflow prediction," Hydrological Processes, vol. 19, no. 19, pp. 3819–3835, 2005.
[13] W. Wang, J. Jin, and Y. Li, "Prediction of inflow at Three Gorges Dam in Yangtze river with wavelet network model," Water Resources Management, vol. 23, no. 13, pp. 2791–2803, 2009.
[14] J. Mata, "Interpretation of concrete dam behaviour with artificial neural network and multiple linear regression models," Engineering Structures, vol. 33, no. 3, pp. 903–910, 2011.
[15] J. Zadheshi, F. Rastegar, F. Sharifi, H. Amini, and H. M. Nasirabad, "Consolidation grouting quality assessment using artificial neural network (ANN)," Indian Geotechnical Journal, vol. 45, no. 2, pp. 136–144, 2015.
[16] F. Umes, M. Demirici, and O. Kisi, "Prediction of mills ferry dam reservoir level in USA using artificial neural network," Periodica Polytechnica-Civil Engineering, vol. 59, no. 3, pp. 309–318, 2015.
[17] X. Li, J. Qiu, Q. Shang, and F. Li, "Simulation of reservoir sediment flushing of the three gorges reservoir using an artificial neural network," Applied Sciences-Basel, vol. 6, no. 5, pp. 1–11, 2016.
[18] A. R. Shaw, H. Smith Sawyer, E. J. Le Boeuf, M. P. McDonald, and B. Hadjerioua, "Hydropower optimization using artificial neural network surrogate models of a high-fidelity hydrodynamics and water quality model," Water Resources Research, vol. 53, no. 11, pp. 9444–9461, 2017.
[19] K.-T. T. Bui, D. Tien Bui, J. Zou, C. Van Doan, and L. Revhaug, "A novel hybrid artificial intelligent approach based on neural fuzzy inference model and particle swarm optimization for horizontal displacement modeling of hydropower dam," Neural Computing and Applications, vol. 29, no. 12, pp. 1495–1506, 2018.
[20] J. Li, X. Chen, C. Gu, and Z. Huo, "Seepage comprehensive evaluation of concrete dam based on grey cluster analysis," Water, vol. 11, no. 7, pp. 1–16, 2019.
[21] J. Qiu, D. Zheng, and K. Zhu, "Seepage monitoring models study of earth-rock dams influenced by rainstorms," Mathematical Problems in Engineering, vol. 2016, Article ID 1656738, 11 pages, 2016.
[22] Q. Pang, S. Wang, and Y. Gu, "Application of earth-rock dam seepage water level model based on hysteresis effect function," Journal of Soil and Water Conservation, vol. 30, no. 2, pp. 225–229, 2016.
[23] B. Wei, M. Gu, H. Li, W. Xiong, and Z. Xu, "Modeling method for predicting seepage of RCC dams considering time-varying and lag effect," Structural Control & Health Monitoring, vol. 25, no. 2, pp. 1–14, 2018.
[24] S.-W. Wang, Y.-L. Xu, C.-S. Gu, and T.-F. Bao, "Monitoring models for base flow effect and daily variation of dam seepage elements considering time lag effect," Water Science and Engineering, vol. 11, no. 4, pp. 344–354, 2018.
[25] X. Cheng, Q. Li, Z. Zhou, Z. Luo, M. Liu, and L. Liu, "Research on a seepage monitoring model of a high core rockfill dam based on machine learning," Sensors, vol. 18, no. 9, pp. 1–14, 2018.
[26] W. Sun and Y. Xu, "Financial security evaluation of the electric power industry in China based on a back propagation neural network optimized by genetic algorithm," Energy, vol. 101, pp. 366–379, 2016.
[27] V. Chandwani, V. Agrawal, and R. Nagar, "Modeling slump of ready mix concrete using genetic algorithms assisted training of artificial neural networks," Expert Systems with Applications, vol. 42, no. 2, pp. 885–893, 2015.
[28] L. Li, Y. Chen, T. Xu, R. Liu, K. Shi, and C. Huang, "Super-resolution mapping of wetland inundation from remote sensing imagery based on integration of back-propagation neural network and genetic algorithm," Remote Sensing of Environment, vol. 164, pp. 142–154, 2015.
[29] S. Nasr, M. El-Shorbagy, I. El-Desoky, Z. Hendawy, and A. Mousa, "Hybrid genetic algorithm for constrained nonlinear optimization problems," British Journal of Mathematics & Computer Science, vol. 7, no. 6, pp. 466–480, 2015.
[30] T. Gulati, M. Chakrabarti, and A. Singh, "Comparative study of response surface methodology, artificial neural network and genetic algorithms for optimization of soybean hydration," Food Technology & Biotechnology, vol. 48, no. 1, pp. 11–18, 2010.
[31] D. Wang, L. Wang, and G. Zhang, "Short-term wind speed forecast model for wind farms based on genetic BP neural network," Journal of Zhejiang University, vol. 46, no. 5, pp. 837–841, 2012.
[32] S. Li, L. Liu, and Y. Xie, "Chaotic prediction for short-term traffic flow of optimized BP neural network based on genetic algorithm," Control and Decision, vol. 26, no. 10, pp. 1581–1585, 2011.
[33] P. Jiang, J. Zhao, and J. Wei, Error Theory and Data Processing, National Defence Industry Press, Beijing, China, 2014.
[34] A. J. Richard, Probability And Statistics For Engineers, Electronics Industry Press, Beijing, China, Ninth edition, 2017.
[35] K. R. Dhawan, S. Burele, and K. Bagwan, "Curtain grouting, a tool used for stopping the seepage from an existing dam," Indian Geotechnical Journal, vol. 49, no. 5, pp. 552–565, 2019.