Modeling Disordered Materials with a High Throughput \textit{ab-initio} Approach

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Predicting material properties of disordered systems remains a long-standing and formidable challenge in rational materials design. To address this issue, we introduce an automated software framework capable of modeling partial occupation within disordered materials using a high-throughput (HT) first principles approach. At the heart of the approach is the construction of supercells containing a virtually equivalent stoichiometry to the disordered material. All unique supercell permutations are enumerated and material properties of each are determined via HT electronic structure calculations. In accordance with a canonical ensemble of supercell states, the framework evaluates ensemble average properties of the system as a function of temperature. As proof of concept, we examine the framework’s final calculated properties of a zinc chalcogenide (ZnS\textsubscript{1−x}Se\textsubscript{x}), a wide-gap oxide semiconductor (Mg\textsubscript{x}Zn\textsubscript{1−x}O), and an iron alloy (Fe\textsubscript{1−x}Cu\textsubscript{x}) at various stoichiometries.

INTRODUCTION

Crystals are characterized by their regular, repeating structures. Such a description allows us to reduce our focus from the macroscopic material to a microscopic subset of unique atoms and positions. A full depiction of material properties, including mechanical, electronic, and magnetic features, follows from an analysis of this primitive lattice. First principles quantum mechanical calculations have been largely successful in reproducing ground state properties of perfectly ordered crystals [1, 2]. However, such perfection does not exist in nature. Instead, crystals display a degree of randomness, or disorder, in their lattices. There are several types of disorder; including topological, spin, substitutional, and vibrational [3]. This work focuses on substitutional disorder, in which crystallographically equivalent sites of a crystal are not uniquely or fully occupied. Rather, each site is characterized by a statistical, or partial, occupation. Such disorder is intrinsic in many technologically significant systems, including those used in fuel cells [4], solar cells [5], high-temperature superconductors [6, 7], low thermal conductivity thermoelectrics [8], imaging and communications devices [9], as well as promising rare-earth free materials for use in free sensors, actuators, energy-harvesters, and spintronic devices [10]. Hence, a comprehensive computational study of substitutionally disordered materials at the atomic scale is of paramount importance for optimizing key physical properties of materials in technological applications.

Unfortunately, structural parameters with partial occupancy cannot be used directly in first principles calculations—a significant hindrance for computational studies of disordered systems. Therefore, additional efforts must be made to model this disorder. One method relies on the reformulation of the disordered system into an average effective virtual compound, \textit{i.e.}, virtual crystal approximation (VCA) [11, 12]. In the VCA approach, each disordered site is treated as a virtual atom possessing attributes that are the compositional-weighted average of the actual occupants. An advantage of the VCA approach is that the computational cost of a disordered material is comparable to that of an ordered material. However, this approach neglects local distortional effects around the partially occupied sites—obscurings fine features of the overall structure.

An alternative method is the mean-field-type coherent potential approximation (CPA) [13], often implemented within the Korringa-Kohn-Rostoker (KKR) [14–16] multiple scattering formalism for enhanced model accuracy [17]. This approach simulates interactions between electrons and the potential via propagators (Green’s functions) and approximates the varying potentials of random alloys by introducing an effective medium potential from a perfectly ordered lattice [18]. Like any mean-field approximation, the CPA description is a single-site approximation and thus unable to resolve short range order effects, such as fine resonance structure in the electronic density of states (DOS).

These approaches, among others [19–21], grapple with the legitimacy of attributing electronic band structure properties to random alloys, which exhibit no translational long range order. This work takes a different approach, reformulating the issue into one of a statistical nature. While not all material properties may be garnered through this reformulation, those that are accessible are of significant practical importance, including the DOS, band gap energy $E_{\text{gap}}$, and magnetic moment $M$.

A rigorous statistical treatment of substitutional disorder at the atomic scale requires utility of large ordered supercells containing a composition consistent with the compound’s stoichiometry [22, 23]. However, the computational cost of such large supercell calculations has traditionally inhibited their use. Fortunately, the emergence
of high-throughput (HT) computational techniques [24] coupled with the exponential growth of computational power is now allowing the study of disordered systems from first principles [25].

Herein, we present an approach to perform such a treatment working within the HT computational framework AFLOW [26, 27]. We highlight three novel and attractive features central to this method: complete implementation into an automatic high throughput framework (optimizing speed without mitigating accuracy), utility of a novel occupancy optimization algorithm, and use of the Universal Force Field method [28] to reduce the number of DFT calculations needed per system.

**METHODOLOGY**

This section details the technicalities of representing a partially occupied disordered system as a series of unique supercells. Here is an outline of the approach:

1. For a given disordered material, optimize its partial occupancy values and determine the size of the derivative superlattices.
2. (a) Use the superlattice size \( n \) to generate a set of unique derivative superlattices and corresponding sets of unique supercells with the required stoichiometry. (b) Import these non-equivalent supercells into the automatic computational framework AFLOW for HT first principles electronic structure calculations.
3. Obtain and use the relative enthalpy of formation to calculate the equilibrium probability of each supercell as a function of temperature \( T \) according to the Boltzmann distribution.
4. Determine the disordered system’s material properties through ensemble averages of the properties calculated for each supercell. Specifically, we will be calculating the system’s density of states (DOS), band gap energy \( E_{\text{gap}} \), and magnetic moment \( M \).

In the following sections, we will refer to a model disordered system, \( \text{Ag}_{8.733}\text{Cd}_{3.8}\text{Zr}_{3.267} \), to illustrate the technical procedures mentioned above. This disordered system has two partially occupied sites: one shared between silver and zirconium, and another shared between cadmium and a vacancy. Working within the AFLOW framework [29], we have designed a simple structure file for partially occupied systems. Adapted from VASP’s POSCAR [30], the PARTCAR contains within it a description of lattice parameters and a list of site coordinates and occupants, along with a concentration tolerance (explained in the next section), and (partial) occupancy values for each site. To see more details about this structure or its PARTCAR, please see the Supplementary Materials.

| \( n \) | Occup. 1 (Ag) | Occup. 2 (Zr) | Occup. 3 (Cd) | \( e_{\text{max}} \) | \( n \) |
|---|---|---|---|---|---|
| 1 | 0.267 | 0.267 | 0.267 | 0.2 | 1 |
| 2 | 0.233 | 0.233 | 0.233 | 0.2 | 2 |
| 3 | 0.067 | 0.067 | 0.133 | 0.133 | 3 |
| 4 | 0.017 | 0.017 | 0.05 | 0.05 | 4 |
| 5 | 0.067 | 0.067 | 0.067 | 0.067 | 5 |
| 6 | 0.067 | 0.067 | 0.033 | 0.067 | 6 |
| 7 | 0.019 | 0.019 | 0.057 | 0.057 | 7 |
| 8 | 0.017 | 0.017 | 0.05 | 0.05 | 4 |
| 9 | 0.044 | 0.044 | 0.022 | 0.044 | 9 |
| 10 | 0.033 | 0.033 | 0.033 | 0.033 | 10 |
| 11 | 0.006 | 0.006 | 0.006 | 0.018 | 11 |
| 12 | 0.017 | 0.017 | 0.033 | 0.033 | 12 |
| 13 | 0.036 | 0.036 | 0.036 | 0.036 | 13 |
| 14 | 0.019 | 0.019 | 0.014 | 0.019 | 14 |
| 15 | 0.00003 | 0.00003 | 0.00003 | 0.00003 | 15 |

**Determine superlattice size**

In order to fully account for the partial occupancy of the disordered system, we would need to generate a set of superlattices of a size corresponding to the lowest common denominator of the fractional partial occupancy values. With partial occupancy values of 0.733 (733/1000) and 0.267 (267/1000) in the disordered system \( \text{Ag}_{8.733}\text{Cd}_{3.8}\text{Zr}_{3.267} \), we would need to construct superlattices of size 1000. Not only would we be working with correspondingly large supercells (16,000 atoms per supercell in our example), but the number of unique supercells in the set would be substantial. This would extend well beyond the capability of first principles calculations, and thus, is not practical. It is therefore necessary to optimize the partial occupancy values to produce an appropriate superlattice size.

We demonstrate utility of an efficient algorithm to calculate the optimized partial occupancy values and corresponding superlattice size with our example disordered system \( \text{Ag}_{8.733}\text{Cd}_{3.8}\text{Zr}_{3.267} \) in Table I. For convenience, we refer to the algorithm’s iteration step as \( n = n' \), the superlattice index, and \( n \) as the superlattice size. Quite simply, the algorithm iterates, increasing the superlattice index from 1 to \( n' \) until the optimized partial occupancy values reach the required accuracy. At each iter-
ation, we generate a fraction for each partially occupied site, all of which have the common denominator $n$. The numerator is determined to be the integer that reduces the overall fraction’s error relative to the actual site’s fractional partial occupancy value. The superlattice size corresponds to the lowest common denominator of the irreducible fractions (e.g. see iteration step 8). The maximum error among all of the sites is chosen to be the accuracy metric for the system.

For the disordered system $\text{Ag}_8\text{Cd}_3\text{Zr}_3$, given a tolerance of 0.01, the calculated superlattice size is 15 (240 atoms per supercell). By choosing a superlattice with a nearly equivalent stoichiometry as the disordered system, we have reduced our supercell size by over a factor of 60 and entered the realm of feasibility with this calculation.

Quite expectedly, we see that the errors in partial occupancy values calculated for silver and zirconium are the same, as they share the same site. The same holds true for cadmium and its vacant counterpart (not shown). Therefore, the algorithm only needs to determine one choice fraction per site, instead of per occupant (as shown). Such an approach reduces computational costs by guaranteeing that only the smallest supercells (both in number and size) with the lowest tolerable error in composition are funneled into our HT first principles calculation framework.

**Unique supercells generation**

With the optimal superlattice size $n$, the unique derivative superlattices of the disordered system can be generated using Hermite Normal Form (HNF) matrices [31]. Each HNF matrix generates a superlattice of a size corresponding to its determinant, $n$. There exists many HNF matrices with the same determinant, each creating a variant superlattice. For each unique superlattice, we generate a complete set of possible supercells with the required stoichiometry by exploring all possible occupations of partially occupied sites. However, not all of these combinations are unique—nominally warranting an involved structure comparison analysis that becomes extremely time consuming for large supercells [31]. Instead, we identify duplicates by estimating the total energy of each supercell in a HT manner based on the Universal Force Field (UFF) method [28]. This classical molecular mechanics force field approximates the energy of a structure by considering its composition, connectivity, and geometry, for which parameters have been tabulated. Only supercells with the same total energy are structurally compared and potentially treated as duplicate structures to be discarded, if necessary. The count of duplicate structures determines the degeneracy of the structure. Only non-equivalent supercells are imported into the automatic computational framework AFLOW for HT quantum mechanics.

**Supercell equilibrium probability calculation**

The unique supercells representing a partially occupied disordered material are labeled as $S_1$, $S_2$, $S_3$, $S_n$. Their formation enthalpies (per atom) are labeled as $H_{F,1}$, $H_{F,2}$, $H_{F,3}$, $H_{F,n}$, respectively. The formation enthalpy of each supercell is automatically calculated from HT first principles calculations using the AFLOW framework [26, 27]. We take the supercell with the lowest formation enthalpy as a reference (ground state structure), and denote its formation enthalpy as $H_{F,0}$. The relative formation enthalpy of the $i$th supercell is calculated as $\Delta H_{F,i} = H_{F,i} - H_{F,0}$ and characterizes its disorder relative to the ground state. The probability $P_i$ of the $i$th supercell is determined by the Boltzmann factor:

$$P_i = \frac{g_i e^{-\Delta H_{F,i}/k_B T}}{\sum_{i=1}^n g_i e^{-\Delta H_{F,i}/k_B T}},$$

where $g_i$ is the degeneracy of the $i$th supercell, $\Delta H_{F,i}$ is the relative formation enthalpy of the $i$th supercell, $k_B$ is the Boltzmann constant, and $T$ is a virtual “roughness” temperature. $T$ is not a true temperature per se, but instead a parameter describing how much disorder has been statistically explored during synthesis. To elaborate further, we consider two extremes in the ensemble average (ignoring structural degeneracy): 1) $k_B T \lesssim \max(\Delta H_{F,i})$ neglecting highly disordered structures ($\Delta H_{F,i} \gg 0$) as $T \to 0$, and 2) $k_B T \gg \max(\Delta H_{F,i})$ representing the annealed limit ($T \to \infty$) in which all structures are considered equiprobable. The probability $P_i$ describes the weight of the $i$th supercell among the thermodynamically equivalent states of the disordered material at equilibrium.

**Ensemble average density of states, band gap energy, and magnetic moment**

With the calculated material properties of each supercell and its equilibrium probability in hand, the overall system properties can be determined as ensemble averages of the properties calculated for each supercell. This work focuses on the calculation of the ensemble average density of states (DOS), band gap energy $E_{\text{gap}}$, and magnetic moment $M$. The DOS of the $i$th supercell is labeled as $N_i(E)$ and indicates the number of electronic states per energy interval. The ensemble average DOS of the system is then determined by the following formula:

$$N(E) = \sum_{i=1}^n P_i \times N_i(E).$$
Additionally, a band gap $E_{\text{gap},i}$ can be extracted from the DOS of each supercell. In this fashion, an ensemble average band gap $E_{\text{gap}}$ can be calculated for the system. It is important to note that standard density functional theory (DFT) calculations are limited to a description of the ground state [1, 2]. Subsequently, calculated excited state properties may contain substantial errors. In particular, DFT tends to underestimate the band gap [32]. Despite these known hindrances in the theory, we demonstrate in the next section that our framework is capable of predicting significant trends specific to the disordered systems. As a bonus, the calculation of these results are performed in a high-throughput fashion. It is expected that a more accurate, fine-grained description of the electronic structure in such systems will be obtained through a combination of our software framework and more advanced first principles approaches [33–39].

In the same spirit as the $N(E)$ and $E_{\text{gap}}$, we consider the calculation of the ensemble average magnetic moment $M$ of the system. The magnetic moment of the $i$th supercell is labeled as $M_i$. If the ground state of the $i$th structure is non-spin-polarized, then its magnetic moment is set to zero, i.e., $M_i = 0$. Taking into account the impact of signed spins on the ensemble average, this approach is limited only to ferromagnetic solutions. Additionally, as an initialization for the self-consistent run, we assume the same ferromagnetic alignment among all of the spins in the system (an AFLOW calculation standard) [26]. Finally, the ensemble average magnetic moment of the system is calculated with the following formula:

$$M = \sum_{i=1}^{n} P_i \times |M_i|.$$ 

**EXAMPLE APPLICATIONS**

To illustrate the effectiveness of our approach, we analyze disordered systems of technological importance: zinc chalcogenides, wide-gap oxide semiconductors, and iron alloys. Unless otherwise stated, the supercells used in our calculations were generated with the lowest superlattice size $n_{\text{scl}}$ needed to represent the composition exactly.

**Zinc chalcogenides**

Over the years, zinc chalcogenides have garnered interest for a dynamic range of applications—beginning with the creation of the first blue-light emitting laser diodes [43], and recently have been studied as inorganic graphene analogues (IGAs) with potential applications in flexible and transparent nanodevices [44]. These wide-gap II-VI semiconductors have demonstrated a smoothly tunable band gap energy $E_{\text{gap}}$ with respect to composition [40–42]. Both linear and quadratic dependencies have been observed, with the latter phenomenon referred to as optical bowing [45]. Specifically, given the pseudoternary system $A_xB_{1-x}C$,

$$E_{\text{gap}}(x) = [x\epsilon_{\text{AC}} + (1-x)\epsilon_{\text{BC}}] - bx(1-x),$$

with $b$ characterizing the bowing. While Larach et al. reported a linear dependence ($b = 0$) [40], Ebina et al. [41] and El-Shazly et al. [42] reported similar bowing parameters of $b = 0.613 \pm 0.027$ eV and $b = 0.457 \pm 0.044$ eV, respectively, averaged over the two observed direct transitions.

As a proof of concept, we utilized our developed disordered system framework to calculate the compositional dependence of the $E_{\text{gap}}$ and DOS for $\text{ZnS}_{1-x}\text{Se}_x$ at room temperature (annealed limit). Overall, this system shows relatively low disorder ($\text{max}(\Delta H_{E,i}) \sim 0.005$ eV), exhibiting negligible variations in the ensemble average properties at higher temperatures. These results, illustrated in Fig. 1, are directly compared against experimental measurements [40–42]. Common among all three trends (Fig. 1(a)) is the $E_{\text{gap}}$ shrinkage with increasing $x_{\text{Se}}$, as well as a near 1 eV tunable $E_{\text{gap}}$ range. Our calculated trend demonstrates a non-zero bowing similar to that observed by both Ebina et al. [41] and El-Shazly et al. [42]. A fit shows a bowing parameter of $b = 0.585 \pm 0.078$ eV, lying in the range between the two experimental bowing parameters.

We also plot the ensemble average DOS plots at room temperature for $x = 0.00$ ($n = 1$), 0.33 ($n = 3$), 0.67 ($n = 3$), and 1.00 ($n = 1$) in Figs. 1(b)-1(e). The plots echo the negatively correlated band gap relationship illustrated in Fig. 1(a), highlighting that the replacement of sulfur with selenium atoms reduces the band gap. Specifically, we observe two phenomena as we increase the concentration of selenium: (red arrows) the reduction of the valence band width (with the exception of $x_{\text{Se}} = 0.00$ (ZnS) concentration), and (blue arrows) a shift of the conduction band peak back towards the Fermi energy. The valence band of ZnS more closely resembles that of its extreme concentration counterpart at $x_{\text{Se}} = 1.00$ (ZnSe) than the others. The extreme concentration conduction peaks appear more defined than their intermediate concentration counterparts, which is likely an artifact of the ensemble averaging calculation.

Finally, we consider a partial-DOS analysis in both species and orbitals (not shown). In the valence band, sulfur and selenium account for the majority of the states, in agreement with their relative concentrations. Meanwhile, zinc accounts for the majority of the states in the conduction band at all concentrations. Correspondingly, at all concentrations, the $p$-orbitals make up the majority of the valence band, whereas the conduction band consists primarily of $s$- and $p$-orbitals. These observations
are consistent with conclusions drawn from previous optical reflectivity measurements that optical transitions are possible from sulfur or selenium valence bands to zinc conduction bands [46].

Overall, our concentration-evolving $E_{\text{gap}}$ trend and DOS plots support a continuing line of work [40–42] corroborating that this system is of the amalgamation type [47] and not of the persistence type [46]. Notably, however, reflectivity spectra shows that the peak position in the $E_{\text{gap}}$ for ZnS rich alloys may remain stationary [41], which may have manifested itself in the aforementioned anomaly observed in this structure’s valence band width.

**Wide-gap oxide semiconductor alloys**

Zinc oxide (ZnO) has proven to be a pervasive material, with far reaching applications such as paints, catalysts, pharmaceuticals (sun creams), and optoelectronics [56]. It has long been investigated for its electronic properties, and falls into the class of transparent conducting oxides [57]. Just as our previous zinc chalcogenide example, ZnO is a wide-gap II-VI semiconductor that has demonstrated a smoothly tunable band gap energy $E_{\text{gap}}$ with composition. In particular, ZnO has been engineered to have an $E_{\text{gap}}$ range as large as 5 eV by synthesizing it with magnesium. This pairing has been intensively studied because of the likeness in ionic radius between zinc and magnesium which results in mitigated misfit strain in the heterostructure [58]. While the solubility of MgO and ZnO is small, synthesis has been made possible throughout the full compositional spectrum [48–55].

As another proof of concept, we model the compositional dependence of the $E_{\text{gap}}$ and DOS for Mg$_x$Zn$_{1-x}$O at room temperature (annealed limit). In particular, we chose this disordered system to illustrate the breath of materials which this framework can model. Similar to ZnS$_{1-x}$Se$_x$, this system shows relatively low disorder ($\Delta H_F \sim 0.007$ eV), exhibiting negligible variations in the ensemble average properties at higher temperatures. We compare our results to that observed empirically [48–55] in Fig. 2. As illustrated in Fig. 2(a), Ohtomo et al. observed a composition dependent phase transition from a wurtzite to a rocksalt structure with increasing $x_{\text{Mg}}$; the transition occurring around the mid concentrations. We mimic this transition in our calculations. Empirically, the overall trend in the wurtzite phase shows a negligible bowing in the $E_{\text{gap}}$ trend, contrasting the significant bowing observed in the rocksalt phase. We note that the wurtzite phase $E_{\text{gap}}$ trend shows a slope of $2.160 \pm 0.080$ eV, while the rocksalt phase shows a bowing parameter of $3.591 \pm 0.856$ eV. Calculated trends are shown in Fig. 2(a). Qualitatively, we also observe linear and non-linear $E_{\text{gap}}$ trends in the wurtzite and rocksalt phases, respectively. The fits were as follows: we observe a slope of $2.147 \pm 0.030$ eV in the wurtzite phase and a bowing parameter of $5.971 \pm 1.835$ eV in the rocksalt phase. These trends match experiment well within the margins of error. We observe a larger margin of error in the rocksalt phase, particular in the phase separated region ($0.4 \lesssim x_{\text{Mg}} \lesssim 0.6$). This may be indicative of the
The magnetic character of the (fcc) \( \gamma \)-Fe phase at low temperatures [63–65], among other complexities in its magnetic phase diagram [66]. One popular approach to studying the \( \gamma \)-Fe phase is through the \( \text{Fe}_{1-x}\text{Cu}_x \) disordered alloy [63, 67, 68]. Nominally, unary copper and iron metals with fcc structures are nonmagnetic, but together exhibit ferromagnetic ordering with very high magnetic moments. This observation has led to identification of Invar and anti-Invar behaviors, which may pave the way to enhanced thermomechanical actuators [63, 67]. \( \text{Fe}_{1-x}\text{Cu}_x \) is an interesting structure in its own right, as it has extremely low miscibility [69].

Overcoming the hurdle of developing metastable structures throughout the full compositional range has been the focus of much research [70]. Such metastable structures have demonstrated novel properties like high thermal and electrical conductivity [71], magnetoresistance, and coercivity [72].

As a final proof of concept, we model the compositional dependence of the magnetic moment \( M \) for \( \text{Fe}_{1-x}\text{Cu}_x \) at \( T = 4.2 \) K for direct comparison against experimental results [59]. Considering both the sensitivity of magnetic properties to temperature as well as the significant disorder exhibited in this system (max (\( \Delta H_{F,i} \) \( \sim \) 1.63 eV)), we limit our analysis to the low temperature limit. This is also where we expect our framework to perform optimally, which considers structures relaxed at zero temperature and pressure [26]. The results are illustrated in Fig. 3. Sumiyama et al. shows that the disordered system’s phase is concentration dependent, with a phase
transition from bcc to fcc in the mid concentrations as $x_{Cu}$ increases. Just as with Mg$_x$Zn$_{1-x}$O, we mimic these observations in our calculation. The overall decreasing trend in $M$ with reduced $x_{Fe}$ in Fig. 3(a) matches our expectations well.

With such a simple system, we also explored whether an augmented superlattice size $n$ enhances our results. While the concentration remains constant for $n$ above that which is needed for the desired concentration $n_{xct}$, more structures are introduced into the ensemble average. The structures themselves also increase in size by a factor of $n$ relative to their parent structure. For $x_{Cu} = 0.2$, 0.4, we simply doubled $n$ ($n_{enh} = 10$), while we tripled $n$ for $x_{Cu} = 0.25$ ($n_{enh} = 12$). With only two two-atom structures needed to describe $x_{Cu} = 0.5$ at $n_{xct}$, we were able to increase $n$ by a factor of five ($n_{enh} = 10$) without compromising the feasibility of the calculation. A comparison of results calculated at $n_{enh}$ is shown in Fig. 3(b). At most concentrations, we observed substantial improvements as our calculated trend more closely follows that which was observed empirically.

Finally, we consider this system’s ensemble average DOS in Fig. 3(c). In general, the DOS near the Fermi energy decreases with increasing $x_{Cu}$, with some instability near the mixed phase regions. This can be understood using the Stoner criterion model for transitional metals [73, 74]. Namely, ferromagnetism appears when the gain in exchange energy is larger than the loss in kinetic energy. A larger DOS at the Fermi energy induces a higher exchange energy and favors a split into the ferromagnetic state. The competition between ferromagnetic and paramagnetic phases can be inferred from the decreasing $M$ trend as depicted in Fig. 3(a).

**ADDITIONAL MATERIALS**

The automated approach to model disordered systems discussed here is implemented with the AFLOW framework [26, 27] and can be downloaded from http://aflowlib.org.

**CONCLUSION**

In this work, we have introduced a software framework capable of modeling substitutionally disordered materials. Specifically, the framework delivers high value properties of disordered systems, including the density of states (DOS), band gap energy $E_{gap}$, and magnetic moment $M$. Though a number of technologically significant examples, we have illustrated the prowess of this highly efficient and convenient framework. Such materials that exhibit highly tunable properties are of critical importance toward the goal of rational materials design. Without loss of feasibility or accuracy, the framework exploits highly successful high-throughput first principles approaches in more complex, real-world systems.

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