DBD transformerless power supplies: impact of the parasitic capacitances on the power transfer.

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Abstract. A new transformerless power supply for DBD application is presented here. The power supply is built with 10kV SiC MOSFET. This high voltage switches allow holding the high voltage required by the DBD. An analytical study of the converter’s operation is presented to deduce the power transmitted to the DBD. A comparison between the experimental and theoretical electrical waveforms is shown. The experimental waveforms are particularly affected by all the parasitic capacitances. When all the switches are in OFF state, oscillations cause over-voltages across the switches. An analysis of the effect of each capacitance is presented and demonstrates that the parasitic capacitances of the switches and of the inductance play a key role in the actual power transfer.

1. Introduction
Dielectric Barrier Discharges (DBD) is a device where it is easy to establish cold plasma at atmospheric pressure [1]. For this reason, DBDs have a lot of applications: ozone generator [2], excimer lamp [3], surface treatment [4], flow control actuators [5]… In Dielectric Barrier Discharge (DBD) setups, at least one dielectric is placed between the two metal electrodes that supply the gas. The dielectric enables to limit the local current of the discharge, even despite a large pd product (p is the pressure and d the gas gap). From an electrical point of view, DBD are capacitive loads. So they must be supplied by an alternative current source. Furthermore, to ignite the discharge at atmospheric pressure, the applied voltage usually reaches several kilovolts. This high alternating voltage is traditionally obtained via amplification, using a step-up transformer. A DBD is a capacitive charge: for a sinusoidal source the current and the voltage are delayed by 90 degree; this implies a high consumption of reactive power and an over-sizing of the transformer in order to sustain the maximum voltage and rms current required by the DBD. Therefore the transformer is often very heavy and cumbersome. For example for a 100W DBD, the volume of the transformer is often up to 1 liter. In classical electronic application this volume is used for a 1kW system. Moreover, the parasitic elements of the transformer (leakage inductance, inter-turn and inter-winding parasitic capacitance), specific to the physical structure of this device, limit the power transfer. For example, parasitic capacitances of the transformer have the same order of magnitude as those of the DBD. They are parallel to the DBD, so they divert a significant part of the current [6]. This also slows down the voltage rise and delays the ignition of the discharge.

Improving these issues and the over-sizing incited us to investigate power supplies for DBD without transformer. A high-voltage inverter is directly connected to the DBD. It involves the use of high-
voltage switches. Because high-voltage switches are available only for a few years, only theoretical developments have been proposed to date [7]. Using 10kV SiC DMOSFET, an innovative transformerless pulsed-current source topology is proposed here and is detailed. The theoretical calculation of the transferred power is presented in a first part. Afterwards we show that the parasitic capacitances affect the operating conditions. We analyze the impact of each parasitic capacitance on the quality of the power transfer. Each capacitance is studied separately in order to understand its impact.

2. Experimental setup and power supplies operating

In a power-supply design approach, the modelling of the DBD is developed below [8]. The DBD used for the experiments is an excimer UV lamp with a cylindrical configuration, with two dielectric barriers and two coaxial tubes of quartz containing a volume of a Xe-Cl gas mixture at 120mBar (Figure 1.a). Metal electrodes are placed on their outer walls. Concerning the geometry of the lamp, the length of the lamp is 115mm and the gap is 20mm.

As long as the discharge is in OFF state, the DBD is modelled by two capacitors in series: $C_{\text{diel}}$ and $C_{\text{gas}}$. The latters correspond respectively to the dielectrics and to the gas capacitance. The geometrical characteristics allow to estimate these capacitances: $C_{\text{gas}}=28\,\text{pF}$ and $C_{\text{diel}}=85\,\text{pF}$. When the discharge is in ON state, we consider that the gas voltage remains constant, $V_{\text{th}}$ (the sign depends on the direction of the current). This assumption is accurate when the discharge is a Townsend or glow mode; it does not take local phenomena into account, but concerns a macroscopic point of view. For a power-supply design approach, it is sufficient to take into account the non-linearity of the plasma [9]. As shown in Figure 1.b the discharge is electrically modelled by a $(V_{\text{gas}}, I_{\text{gas}})$ dipole taking into consideration the non-linearity explained above; this dipole is parallel to the gas capacitance $C_{\text{gas}}$. The breakdown voltage was measured at $V_{\text{th}}=1310\,\text{kV}$. In the whole paper, we develop the analysis with this lamp; however the general conclusions are valid for any DBD device.

Due to the capacitive nature of the DBD and the electrical characteristic of the discharge, the DBD must be supplied by a current source generator [10]. In steady state, the DBD current must have a null average value. Therefore, in the topology presented in Figure 1.b, an inductor is placed in series with the DBD; a constant source voltage $E$ supplies this circuit and the direction of the current depends on the state of the switches.

On the basis of the electrical constraints (voltage and current waveforms) described in the following lines, it can be shown that the characteristics of both semiconductors are those of a thyristor. At the range of the target frequencies (tens of kHz) there is no thyristor on the market, so this function is synthesized by combining in series a MOSFET and a diode [11]. The operation of the converter is presented in Figure 2. In the first sequence (Figure 2.a), the thyristor $Th1$ is closed, thus the high voltage source supplies the resonant $L/C_{eq}$ circuit ($C_{eq}$ correspond to the capacitances $C_{\text{diel}}$ in series with $C_{\text{gas}}$). The DBD current $I_{\text{DBD}}$ and the DBD voltage $V_{\text{DBD}}$ are controlled by the $L/C_{eq}$ circuit until the
gas breakdown. As soon as the discharge is ignited, the gas voltage \( V_{gas} \) remains constant at \( +V_{th} \), and \( I_{DBD} \) and \( V_{DBD} \) are then governed by the resonant loop \( L/C_{diel} \) (Figure 2.b) until \( I_{DBD} \) drops to zero, and the opening of \( Th1 \). The extinction of the discharge results in the opening of the thyristor \( Th1 \). Afterwards, there is no evolution of \( I_{DBD} \) and \( V_{DBD} \) until the closing of \( Th2 \). When \( Th2 \) is turned ON, the DBD and the inductor are short-circuited. The charges accumulated on the dielectric are then used to re-ignite the discharge. The evolution of the electrical waveforms of the DBD is governed by the same resonant circuits: \( L/C_{eq} \) as long as the discharge is OFF (Figure 2.d), and \( L/C_{diel} \) when it is ON (Figure 2.e). The ideal waveforms of \( V_{gas} \) and \( I_{dbd} \) are symmetrical with respect to those obtained in the first half period. An important part of the charges, stored on the dielectrics during (a)-(b), is dissipated in the discharge and the semi-conductors during phase (d)-(e). Therefore in Figure 3 \( V_{DBD} \) voltage may not be symmetrical.

It is important to note that the switch voltage reaches the DBD voltage. In the case of a synthesized thyristor, the MOSFET holds the positive voltage and the diode the negative voltage.

### 3. Theoretical power dissipated in the discharge

The operation of this converter is studied using the state plan analysis [12] from the model shown in Figure 3. This graphical analysis allows building the trajectories of the current-voltage point of a resonant circuit. Assuming that the steady state is reached, on positive half cycle the operating point describes during a first stage (Figure 4.a) a part of a circle centred on \( V_{dbd}=E \) and \( I_{dbd}=0 \), until the gas breakdown (Figure 4.b); at this time, \( V_{gas}=V_{th} \) and the \( V_{dbd} \) voltage takes the \( V_{dbdbr} \) value.

Once the discharge is ignited, the gas capacitance is charged to \( V_{gas}=V_{th} \). During a second stage (Figure 4.c), the part of the circle is centred on \( V_{dbd}=E-V_{th} \) and \( I_{dbd}=I_{dbdbr} \) (Figure 4.d), until \( V_{dbd}=V_{dbd}^{*} \) (\( V_{dbd}^{*} \) voltage when current cancels). In this study, only the positive half-wave is treated. A complete study of the two half periods (work not presented here) has allowed verifying that the current \( I_{dbd} \) is symmetrical.

The maximum DBD voltages of the negative and of the positive halves are respectively referred to \( V_{dbd}^{-} \) and \( V_{dbd}^{+} \). One can notice that \( V_{dbd}^{-}=E-V_{dbd}^{+} \).

Using Figure 4.b and Figure 4.d we can deduce:

\[
V_{dbd}^{+} = \frac{4 \cdot V_{th}^{2} (1+r) - E^{2}}{4 \cdot V_{th} - 2 \cdot E} \tag{1}
\]

With:
The energy $E_n$ dissipated in the discharge during the first half period is:

$$E_n = V_{th} \cdot \int_{t_{breakdown}}^{t_{off}} i_{d} dt = V_{th} \cdot C_{diel} \cdot \left( V_{d} + V_{th} \right) - V_{th} \cdot \left( V_{d} + V_{th} \right)$$

with $t_{breakdown}$ the time of the gas ignition and $t_{off}$ the end of the discharge.

To calculate the energy, we need the expression of $V_{d}$ and $V_{d_{breakdown}}$. When the discharge is ignited (between $t_{breakdown}$ and $t_{off}$) the dielectric voltage is:

$$V_{d} = V_{d_{breakdown}} - V_{th}$$

so we deduce $V_{d_{breakdown}}$:

$$V_{d_{breakdown}} = V_{d} + V_{th}$$

To calculate $V_{d_{breakdown}}$, we need the expression of $V_{d_{breakdown}}$ obtained from the integration of $V_{d}$ between the time of $Th_1$ switching ON ($t=0$) and the time of the gas ignition ($t=t_{breakdown}$):

$$V_{d_{breakdown}} = \int_{V_{d}}^{V_{th}} dV = C_{eq} \int_{t_{breakdown}}^{t_{off}} i_{d} dt$$

So combining the equation (4) and equation (6):

$$V_{d_{breakdown}} = V_{d} + V_{th} \cdot (2 \cdot r + 1)$$

From equations (3), (5) and (7), the energy dissipated in the first half period is:

$$E_n = 2 \cdot C_{gas} \cdot V_{th}^2 \cdot \frac{E}{2 \cdot V_{th} - E}$$

The energy dissipated in the first half period is equal to the energy dissipated in the second half period so the power $P$ dissipated in the discharge is:

$$P = 4 \cdot C_{gas} \cdot f \cdot V_{th}^2 \cdot \frac{E}{2 \cdot V_{th} - E}$$

The evolution of the power dissipated in the discharge $P$ versus the power supply voltage $E$ is plotted in Figure 5. The circuit presented in Figure 1.b is simulated using PLECS. The simulation confirms...
the theoretical equation presented in equation (7). It should be noticed that the inductance has no influence on the power. Its value only adjusts the duration of the discharge and the magnitude of the current.

As long as $E$ is lower than 2000V, the power delivered to the DBD increases slowly. When $E$ tends to $2V_{th}$, the power tends toward the infinity. In this case at the end of each half cycle the dielectric voltage (or the charge stored on the dielectric) are increased. So, the breakdown appears earlier during the period and the maximum current $I_{dibd}$ of the next discharge increased. Steady state cannot be found.

As shown in equation (9), it is possible to adjust the power $P$ by the frequency and by $E$. However, it is important to limit $E$ to a value below lower than $2V_{th}$.

4. Experimental validation

A prototype of this power converter has been realized using high voltage switches: SiC power DMOSFET from CREE with a 10kV maximum drain to source voltage are used. The series connected diodes C4D02120A, holding up to 1700V from CREE are used. Throughout the whole paper (for experiment or for simulation), the inductance value is 17mH. At 30kHz and with the lamp used here, the duration of the pulse is always lower than the half period. Therefore, the switch operates really as a thyristor. The volume and the weight of the power supply are very weak compared to a power supply with a transformer.

The voltages are measured using high-voltage differential probes, TESTEC TT-SI 010 A, and the current is measured using a 4100 Pearson probe. Electrical waveforms are record using a LECROY Wavesurfer 24XS oscilloscope. The constant voltage source $E$ is an adjustable power supply (SFRD0F-2000, Technix brand).

The electrical waveforms ($V_{dibd}$, $I_{dibd}$ and $V_{th1}$), measured at 30kHz and $E=3$ kV, are presented in Figure 6. The time evolution of $V_{dibd}$ is the same as for $V_{th1}$, delayed by a half period. When the discharge turns ON the waveforms are very close to those presented above. According to the previous theoretical analysis, it has been unexpected to observe some oscillations in all the waveforms when the discharge and the switches turn OFF. This is because the diagram of the power supply presented in Figure 1.b is simplistic and does not take into account the parasitic elements. As can be seen, the oscillations cause over-voltage across the semiconductors. This can be a serious issue for transformerless power supply, because high voltages switches must sustain this over-voltage and are currently limited to 10kV.

In Figure 7 we present a simulation model of the power supply taking into account all the parasitic capacitances. The value of the MOSFET capacitance $C_{ossi}$ and of the diode capacitance $C_{di}$ are taken from the datasheet and arranged in a table indexed by semiconductor voltage. The parasitic capacitance of the inductance $C_{para_L}$ is measured by an impedance bridge and is equal to 5pF. The
probe capacitance \( C_{probe} \) is also measured using two current probes (one upstream and one downstream the voltage probe). Finally a parasitic capacitance \( C_{para} \) is inserted between the probe and the DBD. This last parasitic capacitance takes into account the high voltage connection to the DBD (wire, high voltage terminals ...). \( C_{para} \) is measured when the discharge is OFF by a basic current voltage method and its value is 15pF.

![Figure 6: Electrical waveform: comparison between experimental measurement and simulation of the diagram of Figure 7.](image)

The power supply with all the parasitic capacitance presented in Figure 7 is simulated with PLECS. As presented in Figure 6, this simulation accurately fits the measured waveforms: same amplitude, same oscillation frequency. The oscillations observed after the extinction of the discharge are therefore due to the parasitic capacitance presented in Figure 7. If all these parasitic capacitances are not taken into account, the frequency and the amplitude of the oscillations are not accurate. Nevertheless, in order to simplify the analysis, we consider in the following sections separately the role of each parasitic capacitance.

5. Influence of the parasitic capacitance of the switches

In this part we use the basic thyristor model developed by PLECS. For each thyristor, \( Th_1 \) and \( Th_2 \), only a constant capacitance \( C_{p, Th} \) takes into account the parasitic effects as seen in Figure 8. In Figure 10.b, the simulated waveforms of \( V_{DBD}, V_{diel}, V_{Th2} \) and \( i_{Th1} \) are presented for the first half period (when \( Th_2 \) is in OFF state) and for a frequency of 30kHz. When \( Th_1 \) is turned ON, the waveform does not change with or without parasitic capacitances. During this phase, the parasitic capacitance of \( Th_1 \) is short-circuited and the one of \( Th_2 \) is charged to \( E \); no charges are transferred between these parasitic capacitances and other elements of the circuit. As long as \( Th_1 \) is ON, its parasitic capacitance plays no role. When the current of \( Th_1 \) drops to zero, the discharge extinguishes and \( Th_1 \) blocks spontaneously. So all switches are OFF and electric charges move between the DBD and the switches parasitic capacitances. Indeed, voltage is not imposed on \( C_{p, Th} \). The charge transfer leads to oscillations that are visible in all the electrical waveform. Therefore the parasitic capacitances of the switches are the only

![Figure 7: diagram of the power supply tacking into account al the parasitic capacitance.](image)
responsible of these oscillations. It is not shown here, but it is easy to understand that the same phenomenon appears on the second half period (Th₁ remains OFF).

**Figure 8**: Power supply with only the parasitic capacitances of the switches.

In Figure 9, we present the evolution of the power versus the constant voltage \( E \) for a parasitic capacitance \( C_{p, Th} \) of 20\( \text{pF} \) (red curve). This value corresponds to the order of magnitude of a high voltage switch.

**Figure 9**: Power transferred to the discharge. Full line: with a parasitic capacitance of 20 \( \text{pF} \). Dashed line: Without parasitic capacitances (equation (9)).

In Figure 9, we present the evolution of the power versus the constant voltage \( E \) for a parasitic capacitance \( C_{p, Th} \) of 20\( \text{pF} \) (red curve). This value corresponds to the order of magnitude of a high voltage switch.

**Figure 10**: Simulated electrical waveform of the power supply with a parasitic capacitance. First half period when Th₁ turned OFF and Th₂ turned ON. Switching time are indicated (a): \( C_{p, Th}=7.8\text{pF} \). Bracket *: local maxima of \( V_{\text{dielec}} \). Bracket m: local minima of \( V_{\text{dielec}} \). (b): \( C_{p, Th}=13\text{pF} \).

As can be seen in Figure 9, parasitic capacitances of the switches clearly affect the power transferred to the discharge. With switch parasitic capacitances, the power is lower than without switch parasitic capacitances. Moreover with switches parasitic capacitance, the powers do not present a hyperbolic trend when \( E \) is close to \( 2V_{\text{th}} \). The power supply can operate in a wider range of voltage \( E \). Indeed, as soon as all the thyristors are open, the parasitic capacitances of the switches discharge the dielectrics of the DBD. In any case, compared to the theoretical case, fewer charges are stored on the dielectrics when a thyristor is closed. If fewer charges are available to ignite the next discharge, the energy dissipated will be lower. This phenomenon explains why the power dissipated in the discharge with \( C_{p, Th} \) is lower than the power dissipated in the discharge without parasitic capacitances.
Figure 11 presents the evolution of the power transferred to the discharge versus \( C_{p, Th} \) for a frequency of 30 kHz and \( E=3kV \). Overall, the power tends to decrease with \( C_{p, Th} \) but there are local maxima where the power strongly increases.

To understand these power peaks we have to look carefully at the temporal evolution of \( V_{Th2} \) and \( V_{diel} \) presented in Figure 10.a and Figure 10.b. The Figure 10.a corresponds to a power peak, and Figure 10.b corresponds to a power deep. As can be seen, the numbers of local minima and maxima on Figure 10.a and Figure 10.b are different. The parasitic capacitance changes the oscillations frequency and the number of oscillating periods during the OFF time of the discharge (when \( Th1 \) and \( Th2 \) are in OFF state). In some cases, \( Th1 \) is closed when \( V_{diel} \) is maximal and there is a power peak (Figure 10.a), in other cases \( Th2 \) is closed when \( V_{diel} \) is minimal and there is a power deep (Figure 10.b). Therefore we observe a power deep when fewer charges are stored on the dielectric, and at the opposite we observe a power peak when more charges are present on the dielectric. This further regard confirms that the power dissipated in the discharge strongly depends on the charges stored on the dielectric before the closing of the switches.

6. Influence of the voltage probe capacitance

The probe capacitance \( C_{probe} \) or the parasitic capacitance \( C_{para} \) (which consists of the connection and the wire) do not substantially change the situation explained above; their impacts is mainly a change of the resonant frequency that defines the duration of the current pulses.

If the switches parasitic capacitances are not considered, there are no additional oscillations (with respect to the theoretical waveforms of Figure 3) when all the switches are in OFF state; the \( P(E) \) plot (power \( P \) versus \( E \) voltage) keeps the hyperbolic shape presented in Figure 5 and shown again on Figure 9.

With switches parasitic capacitances, the oscillations always exist when both switches are OFF. \( C_{probe} \) affects the oscillation frequency and the \( C_{para} \) or \( C_{probe} \) capacitances shift lightly the curve presented in Figure 11, but do not change fundamentally the operation of the power supply.

Moreover, if a voltage probe is connected to switch terminals, its parasitic capacitance will play the same role as the parasitic capacitance of the switch.
7. Influence of the parasitic capacitance of the inductance

Depending on the presence of the switches capacitances, the parasitic capacitance of the inductance affect markedly the operating of the power supply.

7.1. Without switches parasitic capacitances

We use PLECS to simulate the power supply presented in Figure 1.b but we add a capacitance of $C_{\text{para,L}}=5\,\text{pF}$ in parallel with the inductance. The time evolution of $V_{\text{th2}}, V_{\text{DBD}}, V_{\text{diel}}$ and $I_{\text{bd}}$ is presented in Figure 13. The time evolution of $V_{\text{th1}}$ is the same that the time evolution of $V_{\text{th2}}$ delayed by a half period.

![Figure 12: Charges transfer when all the switches and the discharge are OFF](image)

When all the switches are OFF (Figure 12), the oscillating circuit consists on $L$ in parallel with only $C_{\text{para,L}}$. The moving charges $Q$ are presented in Figure 12. Because all the switches are in OFF state, no current flows through the DBD and the DBD voltage remains constant. The switches voltage is equal to the DBD voltage plus the voltage of oscillating circuit $L/C_{\text{para,L}}$ (Figure 13).

![Figure 13: Electrical waveform with parasitic capacitance of the inductance. $E=2\,\text{kV}, f=30$ kHz.](image)

When one switch is turned ON we observe a current spike on $I_{\text{BD}}$. This is due to a sudden change of the voltage applied on the inductance parasitic capacitance. According to the current ratings of the semiconductor, these spikes could damage the switches. Moreover, when the switching appears, a strong and swift voltage step is directly applied on the series circuit consisting in the DBD and the inductance. Without $C_{\text{para,L}}$, the inductance $L$ sustains the totality of the voltage step. With $C_{\text{para,L}}$, this voltage step is applied to the 3 capacities in series: $C_{\text{para,L}}, C_{\text{gas}}, C_{\text{diel}}$. As we can see in Figure 13, it causes a slight drop of $V_{\text{DBD}}$ and $V_{\text{diel}}$ as soon as $Th_1$ or $Th_2$ turns ON. As explain above, a drop of the dielectric voltage causes a limitation of the power. As shown in Figure 14, with only the parasitic capacitance of the inductance, the power plot $P(E)$ are not an hyperbolic trend; $C_{\text{para,L}}$ limits the power transferred to the discharge.

![Figure 14: Evolution of the power with only an inductance parasitic capacitance $C_{\text{para,L}}=5\,\text{pF}$. $f=30\,\text{kHz}$](image)
7.2. With switches parasitic capacitances
The operating is nearly the same as the one described in the part 5 (with only the parasitic capacitances of the switches). However, the current spike is now present as explained above in 7.1. Due to its low value, $C_{para,L}$ affect scarcely the operation of the power supply on the power transfer.

8. Conclusion
Aimed at limiting the negative effects of the high voltage step up transformer, an innovative transformerless topology for DBD has been proposed. This specific resonant inverter operates as an instantaneous current source and supplies the DBD with positive and negative current pulses. The properties of these pulses (magnitude, duration, frequency $f$, direction) are fully adjustable using the design (values of the circuit's components) and operating degrees of freedom (firing orders, magnitude $E$ of the DC source).

$10kV$ high voltage SiC MOSFETs and diodes are used to synthesize the thyristor-like characteristic of the power switches. These devices, as well as the resonant inductor, introduce parasitic capacitances. The most important points concerning these parasitic capacitances are:

- An increase of the voltage stresses on the semiconductor SiC devices;
- A modification of the output power due to the drop of the charges stored on the dielectrics of the DBD. This charges are diverted to the parasitic capacitances of the switches when the latter are OFF;
- A current spikes in the switches at turn ON, due to the sudden voltage step of the inductance's parasitic capacitance.

As a matter of fact, all these side effects substantially modify the operating conditions of the semiconductors and need to be early accounted at design step. A special care at implementation stage needs to be taken in order to reduce the parasitic capacitances as much as possible.

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