A THERMAL STUDY OF POWER CABLES COOLING IN TUNNELS

F. Boukrouche¹, C. Moreau¹, S. Harmand², F. Beaubert², J. Pellé², O. Moreau³
¹EDF R&D, Moret-sur-Loing, France,
²LAMIH-UMR CNRS 8201, University of Lille Nord de France, France
³EDF – CIST, Paris, France

E-mail: fahd.boukrouche@edf.fr

Abstract. Power transmission through power cables installed in ventilated tunnels has been increasingly used worldwide and offers a complex thermal environment. Established correlations currently in use have been deduced from a non-fully developed turbulent flow. This paper details the experimental investigation of the heat transfer from a single cable in a fully developed turbulent air flow, with emphasis on the effect of the cable spacing from the tunnel wall. Nusselt numbers have been compared for different spacing and velocities. The overall heat transfer is found to be meaningfully lower than in previous studies and no threshold spacing value for the average heat transfer to decrease is clearly found. Thermal radiation is found to greatly impact the cable cooling profile.

Keywords: Power delivery, Forced convection, Radiation, Fully turbulent flow.

Nomenclature

| Symbol | Description | Unit |
|--------|-------------|------|
| \( D_e \) | Cable diameter | \( m \) |
| \( D_h \) | Hydraulic diameter | \( m \) |
| \( U \) | Mean axial velocity | \( m/s \) |
| \( \nu \) | Kinematic viscosity | \( m^2/s \) |
| \( \mu \) | Dynamic viscosity | \( kg/m.s \) |
| \( C_p \) | Specific heat | \( J/kg.K \) |
| \( \lambda \) | Thermal conductivity | \( W/m.K \) |
| \( \theta_s \) | Temperature at azimuthal location on the cable | \( ^\circ C \) |
| \( \theta_{\text{wall}} \) | Wall temperature | \( ^\circ C \) |
| \( \theta_{\text{ambient}} \) | Ambient temperature | \( ^\circ C \) |
| \( \bar{\theta} \) | Mean azimuthal temperature | \( ^\circ C \) |
| \( T_2 \) | Thermal resistance of the heatshrink | \( m^2K/W \) |
| \( P_{\text{tot}} \) | Heating power | \( W/m \) |
| \( P_{\text{conv}} \) | Convective power | \( W/m \) |
| \( P_{\text{ray}} \) | Radiative power | \( W/m \) |
| \( L_e \) | Turbulent entrance length | \( m \) |
| \( a \) | Mock-up width | \( m \) |
| \( \text{Re}_{De} \) | Reynolds number | \( U.D_e/\nu \) |
| \( P_r \) | Prandtl number | \( C_p.\mu/\lambda \) |
| \( \text{Nu}_{De} \) | Local Nusselt number | |
| \( \text{Nu}_{De} \) | Mean azimuthal Nusselt number | |
| \( a/D_e \) | Aspect Ratio | |

Content from this work may be used under the terms of the Creative Commons Attribution 3.0 licence. Any further distribution of this work must maintain attribution to the author(s) and the title of the work, journal citation and DOI.
Published under licence by IOP Publishing Ltd
1. Introduction

Underground power transmission networks are increasingly used across the world. Power cables laid in tunnels are transmitting currents and then, heating the enclosed environment. The precise knowledge of the thermal environment in the tunnels is a key factor in the determination of the permissible current allowed to flow in the link (the cable rating).

Before 1972, this kind of air flow has been treated approximately with classical correlations established for forced convection in pipes as in Dittus–Boelter equation (1).

\[
\overline{Nu_{Dh}} = 0.023 \, Re_{Dh}^{0.8} \, Pr^{0.4} \quad \text{for} \quad Pr > 0.5 \quad \text{and} \quad Re_{Dh} > 10000 \quad (1)
\]

The reference laws for the heat transfer over heated cylinders has been proposed by Weedy and El Zayyat, 1972 [1]. The authors have done extensive testing with dummy cables placed in a wind tunnel of dimensions 2.13x1.67x4.5m, with several cable diameters and velocities from 0 m/s to 6 m/s. Single cable and typical group configurations used in practice have been studied in natural convection as well as forced convection and laws have been obtained in the form of equation (2).

\[
\overline{Nu_{De}} = C \, Re_{De}^{0.65} \quad \text{for} \quad 6.25 \times 10^3 \leq Re_{De} \leq 5.0 \times 10^4 \quad (2)
\]

with Reynolds number based on the cables diameters ranging between \(6.25 \times 10^3\) and \(5.0 \times 10^4\). The coefficient \(C\) is given for single cable and groups of three cables (vertical flat and trefoil formations).

More recent work done by Pilgrim [2] has pointed out the highly insufficient length of the test bench used in [1] to obtain a fully developed turbulent flow, leading to higher heat transfer estimate. Moreover, the presence of cleats to secure the cables to the wall in the middle of the test area act as heat sinks and break the development of the dynamic and thermal boundary layers. These factors would participate in the overestimation of the convective heat transfer coefficient and therefore the Nusselt correlation associated.

From a theoretical point of view, flows over long cylinders have been scarcely studied. [3][4] have studied the heat transfer from a heated cylinder of small size and concentric configurations with high aspect ratio \(D_{\text{enclosure}}/D_{\text{cylinder}}\). More information is available on the natural convection of enclosed cylinder, [5][6] have studied natural convection in an enclosed cylinder of small aspect ratio.

In order to have a better understanding of the heat transfer phenomena occurring with power cables installed in ventilated tunnels, an expurgated experimental study has been proposed. The key concerns have been allowing an appropriate entrance length for the turbulent flow and as little perturbation to the air flow as possible. The Nusselt laws derived from these tests would serve as a basis for more complex setup.

The paper presents the experimental setup used in this scope, and the experimental protocol is detailed. The results are then discussed in terms of overall heat transfer before emphasising on the local behaviour in near wall configurations.
2. Experimental setup

2.1. Experimental apparatus

A tunnel mock-up has been designed in similitude with an actual power tunnel. Reynolds number based on the cable diameter range between $1.25 \times 10^4$ and $5.5 \times 10^4$. The original tunnel square section is represented by a 0.333 m square section and the mock-up length is 6.5 m long. The aspect ratio for a single cable configuration is $D_e/\alpha = 11.5$. The dimensions are set for the maximum entrance length to be of 6 m for the maximum Reynolds number tested.

![Figure 2: Test bench and vacuum fan (left); Flow direction and measurement emplacement (right)](image)

0.029 m diameter dummy cables are made of an aluminium core, a ceramic body and two heatshrink polyethylene (PE) outer jackets, the same material that is used for power cables outer sheath. These cables have been instrumented with ten thermocouples (T-type, ±0.5 °C) placed in grooves at the ceramic surface in a section located at 0.7 m from the cable end. The grooves were filled with ceramic mortar with equivalent thermal characteristics as the cable body. The dimensions (tunnel length and section, cables diameters) have been set to assure a fully turbulent flow at the measurement section. The heat is generated by an alternating current flow up to 600 A through the cables. The current is measured with an instrument transformer (±0.5 %) and the electrical resistivity is measured with a four-point probe method (±0.25 % + 25 μΩ).

![Figure 3: Dummy cable – Centered configuration (left); cable details (middle); near wall configuration (right)](image)
2.2. Test protocol
The single cable configuration has been tested at $L_x = 5.7De$ (middle of the test section) and at spacing values of $L_x = 2De$, $L_x = 1De$ and $L_x = 0.5De$ from the tunnel wall (see Figure 1). The current value (heat generation) is adapted in order to keep the cable at a constant surface temperature whatever the spacing value and the velocity used in the tunnel.

The tests are done at six Reynolds numbers with the air flow generated by a blower functioning on exhaust. A velocity profile at the section used for the measurements has been done by pitot tube for the six flow regime tested. Air temperature and the cable core temperature are monitored respectively by thermocouples type K ($\mp 1°C$) and type T shielded (to prevent perturbation of the measures by the transiting current).

The local Nusselt numbers are deduced from experimental data by equation (3) below with air properties calculated at bulk temperature

$$Nu_{De} = \left(\frac{D_e}{\lambda}\pi D_e(\theta_s - \theta_{ambient})\right) \frac{P_{conv}}{P_{conv} + P_{ray}}$$

with $\theta_s = \theta - \frac{1}{10}T_2P_{tot}$

where $\theta$ is the local temperature ($°C$). The mean azimuthal Nusselt number are calculated with the ten data points by equation (4)

$$\bar{Nu}_{De} = \frac{D_e}{2\pi \lambda(\theta_s - \theta_{ambient})} \int_0^{2\pi} P_{conv}(\varphi) d\varphi$$

The radiative contribution to the heat transfer is subtracted from the total power for each data points. A 2D numerical simulation using COMSOL Multiphysics® is realized for each configuration. The fast hemicube algorithm is used to compute the view factors, which is advantageously fast to produce an approximate value [7]. The Experimental temperature profiles are used as boundary conditions on the tunnel walls and on the PE-sheat/ceramic interface. The thermal equilibrium is computed and the radiative heat flux is extracted and used to compute the convective exchange.

3. Results and discussions
3.1. Radiative contribution to the heat transfer
The impact of the wall on the cable radiative heat transfer can be observed in the Figures 4. The radiative cooling is decreasing with the spacing value which is explained by two factors: first, the reduced surface with which the part of the cable surface in close proximity with the tunnel can radiate heat. Second, the overheating of the nearest wall facing the cable when the steady-state is reached. The radiation exchange is then less important with the already hot surface (see wall temperature measurements in Figure 5).
The radiosity method calculation [8] and COMSOL simulations of the radiative exchange between the cable and the walls have shown the radiative losses to be up to 30% of the total heat loss, then decreasing as the Reynolds number rises. These percentages stay fairly constant for every configuration.

3.2. Mean azimuthal Nusselt number

The mean azimuthal heat transfer for the three configurations are presented in the Figure 8 below. Nusselt correlations are obtained by power law trend curves and are compared with the power law from [1], first with the given C constant for a single cable (C = 0.13), then choosing the constant for the best fit. Measurement uncertainties on the Nusselt values range from 11% to 13%.

The Figure 7 compares the experimental results with the power law proposed by [1]. Nusselt values are found to be meaningfully lower than the ones expected from the correlation. This can be explained by two factors: the difference in aspect ratio, 11.4 in this study, in-between (15.3 – 40) for the correlation presented in [1]. The effect of having turbulent flow without any perturbations from a support and a sufficient length for the thermal boundary layer to develop, thus reducing the heat transfer as the temperature gradients stabilize themselves along the cable length as explained by Pilgrim [2].
The kind of power law from [1] can be used to fit the experimental data within the error margins. Below, the Figures present two fitting curves for the experimental data, one based on the correlation of [1] with a constant matching the data, and a power curve fitting curve calculated directly by the least square method. A good match of the correlation of Weedy and El Zayyat [1] is found for the 1De and 2De positions (power of respectively 0.65 and 0.66) but it is far less accurate for the 5.7De and 0.5De as the least square fitting returns power respectively of 0.73 and 0.75.

\[
\begin{align*}
N_u_{De} &= 0.13 R_{ReDe}^{0.65} \\
N_u_{De} &= 0.0202 R_{ReDe}^{0.73} \\
N_u_{De} &= 0.039 R_{ReDe}^{0.66} \\
N_u_{De} &= 0.045 R_{ReDe}^{0.65}
\end{align*}
\]

\[R^2 = 0.9924\]

\[R^2 = 0.9849\]

Figure 7: Comparison of experimental overall Nusselt numbers with [1] – 5.7De cable position –
The Figure 9 presents the least-square curves-fitting data for all Lx values. No threshold value is clearly found for the mean azimuthal heat transfer even if a slight decrease of the Nusselt curves can be observed for 2De and 1De. The higher levels observed for the 0.5De position is within the uncertainty margins of the 5.7De curve. The heat transfer for the 0.5De position is still superior in comparison to 2De and 1De positions.
4. Conclusion

The forced convection over long cylinder surfaces has been studied and compared with the existing empirical model made for a single cable configuration. No clear threshold value for thermal independency is found as in [1] but experimental data showed an overestimation which can be accounted for the particularity of the experimental setup used in [1], those being an undeveloped turbulent flow and the presence of racks for supports. The effect of the wall spacing has also shown a cooling profile that cannot be accounted for with the sole forced convection, which led to an investigation of the radiative heat transfer contribution of the cable portion facing the closest tunnel wall. A rise in the temperature of the tunnel wall has been found while the other walls stay close to room temperature and the radiative contribution to the heat transfer has been found to be significant.

A more complete radiative study of the experimental configurations is currently under way involving measurements for the radiative heat flux of the cable. Several other cable configurations, involving two and three cables are studied to assess the impact of a cable group on the cooling profiles.

References
[1] B.M Weedy and H.M El Zayyat 1972, Heat Transfer From Cables In Tunnels Ans Shafts, IEEE-PES
[2] J Pilgrim 2001, Circuit Rating Methods For High Temperature Cables (Doctoral thesis, University of Southampton, Electronics and Computer Science: EEE), retrieved from http://eprints.soton.ac.uk/195003/
[3] A Shedaghat and F Léon 2013, Thermal Analysis of Power Cables in Free Air: Evaluation and Improvement of IEC Standard Ampacity Calculations, IEEE PES
[4] R Wiberg and N Lior 2004, Heat Transfer from a cylinder in axial turbulent flows, International Journal of heat and Mass Transfer
[5] P Teerstra and M.M Yovanovich 1998, Comprehensive Review of Natural Convection in Horizontal Circular Annuli, ASME
[6] S.K.S Boetcher 2014, Natural Convection from Circular Cylinders, SpringerBriefs in Thermal Engineering and Applied Science
[7] B Watel, S Harmand, B Desmet 1999, Influence of Flow Velocity and Fin Spacing on the Forced Convective Heat Transfer from an Annular-Finned Tube, JSME International Journal
[8] H.E Dillion, A.F Emery, R.J Cochran, A.M.Mescher 2014, Validation of Radiation Computations using Viewfactors and COMSOL's Hemicube Approaches, COMSOL User Conference