Optical forces on cylinders near subwavelength slits illuminated
by a photonic nanojet

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Abstract

We discuss optical forces exerted on particles, either dielectric or metallic, near a subwavelength slit illuminated by a photonic nanojet. We compare those cases in which the Mie resonances are or are not excited. The configurations on study are 2D, hence those particles are infinite cylinders and, in order to obtain extraordinary transmission, the illuminating beam is p-polarized. We show the different effects of these particle resonances on the optical forces: while whispering gallery modes under those illumination conditions weaken the force strength, this latter is enhanced by localized plasmon excitation. Also, illuminating the slit with a nanojet enhances the optical forces on the particle at the exit of the aperture by a factor between 3 and 10 compared with illumination of the slit with a Gaussian beam. In addition, the pulling force that such a small resonant metallic particle suffers on direct illumination by a nanojet, can change by the presence of the slit, so that it may become repulsive at certain lateral positions of the particle.
INTRODUCTION

Studies on optical forces on micro and nano-objects, both in their applications to trapping as well as to optical binding, show the sensitivity of these techniques to the thermal action on the kinetics of these systems. This involves to increase both the numerical aperture NA and the power of the illuminating beam to control the experiments; the former procedure has obvious limitations for the manipulation of biological specimens.

The effectiveness of optical trapping increases by illuminating particles through subwavelength apertures in supertransmission, namely on excitation of the aperture morphology dependent resonances (MDR). This allows lower illumination powers and its performance is greatly improved when also the Mie resonances of the particles are excited, i.e. their whispering gallery modes (WGM) or localized surface plasmons (LSP). This enhances the aperture transmittance and localization of light.

Nevertheless, illuminating with photonic nanojets (PNJ) constitutes an alternative means to enhance that transmission and localization of light through apertures. PNJs have subwavelength spatial resolution and hence are of great interest for microscopy and detection at the nanoscale. Since however they are nonresonant focusing effects, their appearance is not so narrowly constrained by the constitutive parameters and morphology of the particles as Mie resonances are.

As far as we know, in contrast with the extensive study on nanojets, there is only one report concerning optical forces on a metallic particle close to a PNJ. We thus present here an analysis on the effect that the presence of subwavelength apertures has on these forces; a subject that combines the phenomenon of extraordinary transmission with the nanojet focusing and localization of optical energy, and which has never been addressed. The nanoparticle is either dielectric or metallic, and its MDRs may be excited.

We shall employ 2D configurations, so that the particles are cylinders with cross section in the plane of calculations, and the apertures are slits. It is well-known that this accounts for the main features of the phenomenon providing one does not look for depolarization effects and it is certainly the case for PNJs. Therefore in order to obtain slit supertransmission, the incident wave is p-polarized.

We will employ the Maxwell stress tensor (MST). The fields are calculated by a finite element method. Section 2 accounts for these computations as well as for
those of the energies and electromagnetic forces, whose details were given in our previous works [14, 38, 44].

Then we shall analyze in Sections 3 and 4 the effects of exciting a WGM in a Si cylinder and a LSP in an Ag one, respectively, on the optical forces exerted on them. This is carried out on comparing the effect of PNJ illumination with and without a subwavelength slit. In this way we shall show that whereas a metallic particle as small as that addressed here, resonantly illuminated by a nanojet, suffers an attractive vertical force, (this is in contrast with previous results [48] concerning larger metallic particles), which makes the nanojet forming cylinder a photonic tractor, the additional presence of a subwavelength aperture may change the sign of this force thus transforming it to repulsive, depending on the lateral position of the cylinder.

In addition, if we previously showed [14] that the presence of the slit enhances the gradient forces by two orders of magnitude compared with the direct illumination of the probe particle by a Gaussian beam of a conventional optical tweezer, we now observe that illuminating the slit with a nanojet increases the magnitude of the optical forces on the particle by a factor between 3 and 10 compared with illumination of the slit with a Gaussian beam.

**NUMERICAL CALCULATIONS**

The calculation of the electromagnetic fields interacting with particles placed at each side of an aperture in a metal slab is now discussed. 2D numerical simulations are done by means of a finite element method (FE) (FEMLAB 3.0a of COMSOL, http://www.comsol.com). Aside polarization effects, the main features of the physical process of coupling, resonance excitation and nanojet focalization are analogous to those in 3D; this was already analyzed for nanojets in [40–43]. Technical details on the calculations have been given in [14, 38, 56].

Although other materials can be chosen, Si and Ag have been used to simulate the probe particles, performing the analysis on the grounds of their rich Mie resonance spectra in the studied regimes, (near IR and near UV, respectively). The dielectric material for the nanojet-focusing particle is SiO$_2$ – glass [57, 58]. The reason of working with either dielectric or metallic particles is to see the effects of their Mie resonances on the induced electromagnetic forces, taking into account the influence of the presence of a subwavelength slit illuminated by the nanojet. As in previous works, and because of the same reasons
the latter is considered in a thick Al slab. Noble metals like Au or Ag may be used for thinner slabs.

Following the scheme shown in Fig. 1, an incident beam, linearly p-polarized, namely with its magnetic vector $\mathbf{H}_z$ perpendicular to the XY-plane is launched upwards, propagating in the Y direction. This choice is because p-polarization, in contrast with s-polarization, produces homogeneous eigenmodes, i.e., those which lead to extraordinary transmission of the subwavelength slit [38, 44, 60–62]. The light beam incides on a dielectric cylinder of radius $r_{nj}$, which concentrates a nanojet near its back surface. The nanojet illuminates either the probe cylinder of radius $r$ when the slab in Fig. 1 does not exist; or, when the latter is present, this illumination is done on transmission of the nanojet through the slit, as seen in Fig. 1. The nomenclature followed to classify both localized surface plasmons (LSP) and whispering gallery modes (WGM) of the probe cylinders, as well as the resonances of the slit is: subscripts $(i, j)$, $i$ and $j$ standing for their angular $i$-th and radial $j$-th orders, respectively. In the case of the supertransmission resonances of the slit alone the subscripts $(u, v)$ will be used, $u$ and $v$ standing for their longitudinal $u$-th and transversal $v$-th orders.

In all cases the beam profile at frequency $\omega$ is Gaussian, with magnetic field distribution at its focal plane: $\mathbf{H}_z(x, y) = |\mathbf{H}_{z0}| \exp(-x^2/2\sigma^2) \exp(i((2\pi/\lambda)y - \omega t))$, $|\mathbf{H}_{z0}|$ denoting the modulus amplitude, $2^{1/2}\sigma$ being the half width at half maximum (HWHM) of the beam, and $\lambda$ representing its wavelength. In this way the beam has intensity $(1/\pi)mW/\mu m^2$ and $HWHM = 2r_{nj}$. The geometrical parameters of the cylinders and of the slit have been adjusted such that at the given illuminating wavelength $\lambda$, there is focalization of nanojets as well as excitation of morphology-dependent resonances of both the slit and the probe particle.

The physical quantities shown in the images of the configurations under study are the magnetic field $\mathbf{H}_z(x, y)$, the electric field $\mathbf{E}(x, y)$ and the time-averaged energy flow $\langle S(x, y) \rangle$. The curves presenting the nanojet intensity focused near the back surface of the $SiO_2$ - glass cylinder, are obtained at the point $(x, y)$ where $|\langle S(x, y) \rangle|$ is maximum.

The light concentration either in or on the probe cylinder according to whether this is dielectric or metallic, is evaluated by integrating $|\langle S(x, y) \rangle|$ in a circle which coincides with the circle cross section of the probe cylinder of radius $r$ when this latter is dielectric, or in an annulus surrounding it of radii $r$ and $r_{jm}$ when the probe cylinder is metallic, see
FIG. 1. Schematic illustration of the geometry for the calculation of the slit transmittance and optical force calculations: An incident p-polarized plane wave with a Gaussian profile, (amplitude $A = (1/\pi) mW/\mu m^2$, width of its intensity $\sigma = r_{nj}$), magnetic vector $H_z$ and time-averaged Poynting vector $<S_y>$ impinges a $SiO_2$ – glass cylinder of radius $r_{nj}$ which focuses a nanojet near its back surface, whose intensity is calculated at the point where $|<S_y>|$ is maximum. This nanojet illuminates, either directly or by interposing a subwavelength aperture of width $d$, a cylinder of radius $r$. The aperture is practiced in an $Al$ slab of width $D$ and thickness $h$. The width $D$ is also that of the horizontal side of the simulation window, whose boundary conditions are set to “low reflection”, except in those segments which coincide with the exterior limits of the slab, where “perfect conductor” conditions are set. The intensity focused by the nanojet on the cylinder of radius $r$, either directly or on transmission through the slit, is evaluated as follows: For dielectric ($Si$) particles, the time averaged energy flow norm $|<S_y>|$ is integrated inside the cylinder circle cross section of radius $r$. For metallic ($Ag$) cylinders, one determines $|<S_y>|$ integrated in an annulus of exterior and interior radii: $r_e$ and $r$, respectively. As a beam of unit amplitude is always launched on the system, all transmission graphics presented in this work are normalized to this value. The circumference $\Sigma$ of radius $r_e$, is also used to calculate the electromagnetic forces on the probe particle (see also [14]), no matter whether the cylinder is dielectric or metallic. When there is no upper probe cylinder, the transmittance is obtained on integration of $|<S_y(x,y)>|$ in a circle in vacuum which coincides with that of the probe cylinder cross section.
This stems from the fact that if the particle is dielectric the intensity transmitted by the slit, that couples to the particle WGM, is concentrated inside the cylinder; whereas when this nanoparticle is metallic, this transmitted intensity, coupled to a LSP, remains on the particle surface. On the other hand, the transmittance of the slab when the probe particle is not present is calculated on integration of $|<\mathbf{S}(x,y)>|$ in a circle of radius $r$ in void space which coincides with that of the probe cylinder cross section. In all cases these intensities are normalized to the maximum intensity of the incident Gaussian beam $|<\mathbf{S}_{max}>| = (1/\pi) mW/\mu m^2$.

The time-averaged force on the probe cylinder is calculated by employing the Maxwell stress tensor (MST) [60]:

$$<\mathbf{F}_{em}> = \int \int \left[ \epsilon/2 \text{Re}\{ (\mathbf{E} \cdot \mathbf{n})\mathbf{E}^* \} - \epsilon/4 (\mathbf{E} \cdot \mathbf{E}^*) \mathbf{n} + \mu/2 \text{Re}\{ (\mathbf{H} \cdot \mathbf{n})\mathbf{H}^* \} ight. - \left. \mu/4 (\mathbf{H} \cdot \mathbf{H}^*) \mathbf{n} \right] ds,$$

where the surface of integration $\Sigma$ surrounds the particle as seen in Fig. 1 and $\mathbf{n}$ represents the outward unit normal. In our 2D geometry, $\Sigma$ is the circumference of radius $r_e$, (see Fig. 1). $\epsilon = \mu = 1$.

In Eq. (1), $\mathbf{E}, \mathbf{H}$ and $\mathbf{E}^*, \mathbf{H}^*$ are the values of the fields and their complex conjugates, $\epsilon$ and $\mu$ denotes the electric permittivity and magnetic permeability of the surrounding medium, which in this work will be assumed to be vacuum.

The calculation with FEMLAB of the complex values $\mathbf{E}(r)$ and $\mathbf{H}(r)$ and of the real physical fields: $\mathbf{E}^R(r,t) = \text{Re}[\mathbf{E}(r) \exp(-i\omega t)]$ and $\mathbf{H}^R(r,t) = \text{Re}[\mathbf{H}(r) \exp(-i\omega t)]$, are not straightforward. The details of the procedure have been given in [14].

EXTRAORDINARY TRANSMISSION OF A SLIT IN PRESENCE OF A NANOJET. EXCITATION OF A WHISPERING GALLERY MODE

Excitation of a WGM in a cylinder by nanojet focalization. Effects of coupling by supertransmission

In order to interpret the optical forces on the probe particles, we first discuss the fields resulting from the interaction. We begin dealing with the situation in which the slit is
illuminated by a nanojet in the infrared region. The probe cylinder on the slit exit being dielectric. This makes it possible two processes of supertransmission enhancement: one due to the nanojet focused near the back surface of the dielectric cylinder of radius $r_{nj}$ at the entrance of the aperture, and that resulting from the coupling between the light exiting the slit and the WGM excited in the probe cylinder of radius $r$, (see Fig. 1).

![Graph A](image1.png)

![Graph B](image2.png)

![Graph C](image3.png)

**FIG. 2.** (a) Time-averaged energy flow norm $|<S(r)>|$, transmitted by the slit against illumination wavelength of: a slit alone (width $d = 428.8\,nm$) practiced in an Al slab (width $D = 19.920\,\mu m$, thickness $h = 857.6\,nm$) (black squared curve, values in right vertical axis); and of the same slit illuminated by a nanojet focused near the back surface of a $SiO_2$ − glass cylinder of radius $r_{nj} = 3\,\mu m$ placed at the entrance of this slit (green triangle curve, values in left vertical axis). The red circle curve (values in left vertical axis) stands for $|<S(r)>|$ concentrated by the nanojet at its maximum intensity point when the slab is absent. The calculations are done as explained in Fig. 1. (b) Detail of the electric field $|E(r)|$ magnitude transmission (colors) and vector (arrows) of the nanojet focused near the back surface of the $SiO_2$ − glass cylinder at $\lambda = 1175\,nm$, without slit nor Si probe particle. This corresponds to a peak of the red circle line of (a). (c) The same detail as in (b) but of the time-averaged energy flow $<S(r)>$, (norm in colors and vector in arrows).

We first make a study of the fields and energy without the probe Si. Fig. 2(a) shows the black squared and green triangled curves which stand for the average energy flow, either
when the Gaussian beam directly illuminates the Al slab without the presence of the nanojet, (peak at $\lambda = 1175\text{nm}$), or when the incident light is focused as a nanojet near the back surface of a $SiO_2$ - glass cylinder of radius $r_{nj} = 3\mu m$ placed at the slit entrance. The intensity at that point of the nanojet where it is maximum, without slab, is plotted as the red circle curve. The presence of the nanojet enhances the transmittance peak of the slit by a factor above 4 (at $\lambda = 1155\text{nm}$), but erases the supertransmitted energy peak profile of the slit alone (compare the green triangle and the black square lines), manifesting the non resonant nature of the PNJ focusing process (see the red circle line). A detail of the nanojet alone, i.e. without slit nor Si cylinder, near the back surface of the cylinder is displayed both by its electric field $E(r)$ distribution [see Fig. 2(b)] and by that of its energy flow $< S(r) >$ [Fig. 2(c)], both maps clearly show the focalization process and the interesting vortex of electric field lines about the nanojet focus.

Next, the Si probe cylinder is placed above the $SiO_2$ - glass without the presence of the slit. The light in the Si cylinder now concentrates in the form of a $WGH_{2,1}$ resonance, as shown by the dipolar map of the magnetic field norm $|H(r)|$ in Fig. 3(a), $r = (x, y)$. Consequently, the electric field $E(r)$ distribution acquires a vortex pattern near the probe cylinder [cf. Fig. 3(b)] and, under this incident p-polarization, the light intensity from the nanojet is strongly localized within this Si cylinder [see Fig. 3(c)].

Figure 4(a) shows the average energy flow for all the configurations studied in this paper. The intensity of the nanojet localized in the Si cylinder of radius $r_{nj} = 3\mu m$, without slit, is plotted in the blue curve with triangles down. The peaks of this curve coincide with those of the intensity peak point of the nanojet alone, [see the red curve with circles in Fig. 2(a)], but now enhanced by the resonant concentration due to the $WGH_{2,1}$ resonance at $\lambda = 1175\text{nm}$. As seen, this nanojet also enhances the energy associated to the cylinder resonance by a factor of 10, [cf. the blue curve with triangles down in Fig. 4(a)], on comparing with the case of the resonant Si cylinder directly illuminated by the Gaussian beam without nanojet nor slit, (whose intensity integrated in the Si cylinder cross-section has a maximum at $\lambda = 1195\text{nm}$; not shown here for brevity).

Concerning the nanojet focused in the Al slit with the Si cylinder at its exit, the transmitted intensity inside that cylinder against wavelength takes the form of the pink curve with rotated triangles of Fig. 4(a). This follows the trend of the intensity in that cylinder alone, (not shown here), modulated by that of the nanojet-slit system, as a result of the
FIG. 3. (a) Detail of the map of the magnetic field norm $|\mathbf{H}(r)|$, $\mathbf{r} = (x, y)$, in a resonant Si cylinder of radius $r = 200nm$ illuminated by the nanojet focused at 350nm near the back surface of the $SiO_2$ – glass cylinder of radius $r_{nj} = 3 \mu m$. The Si cylinder is placed at the maximum intensity point of the nanojet. There is energy concentration as a $WGH_{2,1}$ mode of the Si cylinder. (b) Detail of the electric field $\mathbf{E}(\mathbf{r})$ magnitude and vector, (colors and arrows, respectively). (c) Detail of time-averaged energy flow $\langle \mathbf{S}(\mathbf{r}) \rangle$, (norm in colors and vector in arrows). The conditions of illumination in these images are those of Figs. 2(b) - (c) and at the same wavelength.

Effect of nanojet focalization plus WGM resonance excitation. This shows a modest increase of transmitted intensity inside the $Si$ particle (cf. the pink curve with rotated triangles) comparing with that of the nanojet large cylinder plus slit, without the $Si$ particle, (cf. the green curve with triangles up). Nevertheless, the enhancement factor is now above 4 (at $\lambda = 1160nm$) with respect to the transmitted intensity from the slit alone, [cf. black curve with squares in Fig. 2(a)].

A detail of the spatial distributions of $\mathbf{E}$ and $\langle \mathbf{S} \rangle$ at the optimum wavelength for largest transmitted intensity of the system constituted by the large $SiO_2$ – glass cylinder, the subwavelength slit and the resonant $Si$ probe cylinder, can be seen in Figs. 4(b) and 4(c), respectively, showing the vortex of the electric vector in the $Si$ cylinder around the point of maximum intensity concentration. Also, the large charge localization in the corners
FIG. 4. (a) Transmitted time-averaged energy flow norm $|<S(r)>|$ versus illumination wavelength of the following configurations: A nanojet focused by the SiO$_2$–glass cylinder of radius $r_{nj} = 3\mu m$, tangent to the entrance plane of the slit practiced in the Al slab studied in Fig. 2(a), (green curve with up-triangles). A probe Si cylinder is added, tangent to the exit plane of the slit illuminated by the nanojet (pink curve with rotated triangles). The blue curve with down-triangles stands for $|<S(r)>|$ concentrated in the resonant Si cylinder, placed above the nanojet-focusing SiO$_2$–glass one, when there is no slab between them. All these curves are obtained as explained in Fig. 1. (b) Detail of the electric field $E(r)$ magnitude and vector (colors and arrows) in the Si cylinder at the exit plane of the slit illuminated by the nanojet, (see in (a) the pink curve with rotated triangles). The illumination of the nanojet forming large SiO$_2$–glass cylinder below the slit is with a Gaussian beam at $\lambda = 1160nm$. This cylinder is not shown in the figure. (c) The same as in (b) for $<S(r)>$, norm in colors and vector in arrows.

of the slit is clearly observed. This will be seen to have important consequences for the optical forces on the Si cylinder.
Electromagnetic forces on a dielectric cylinder with a whispering gallery mode excited by a nanojet, either directly or on transmission through a subwavelength slit.

Next, we study the force that the electromagnetic fields of the nanojet transmitted through the slit exert on the probe Si cylinder placed at the slit exit.

![Graphs showing force variation](image)

**FIG. 5.** (a) X- and Y-components of the total electromagnetic force $F^t$ on the Si cylinder as it laterally moves to the right from the point of maximum intensity of the nanojet focused by the SiO$_2$−glass cylinder of radius $r_{nj} = 3\mu m$. This point is at 350nm from the back surface of this SiO$_2$−glass cylinder. No slit is present. (b) The same quantities when the Si cylinder separates vertically from the same point as in (a). In both graphics, black squares and green up-triangles curves stand for $F^t_x$ when the Si cylinder is non-resonant ($\lambda = 1280nm$) and when it is resonant ($\lambda = 1175nm$), respectively. Red circle and blue down-triangles represent, in the same order, $F^t_y$.

Figure 5(a) shows the variation in the X- and Y-components of this force when the particle moves horizontally from the peak point of the nanojet intensity map. In this case we assume no slit present. The particle, illuminated out of resonance, is gradually and increasingly attracted along the lateral direction by the gradient of intensity of the nanojet spatial distribution, and less and less pushed vertically, (cf. black squared and red circled curves, respectively). On the other hand, when the $WGH_2,1$ is excited, the particle is now slightly more and more laterally repelled from the peak intensity point of the nanojet map, (see the green up-triangle curve) and weakly, although increasingly and progressively, pushed in the vertical direction (cf. blue-down triangle curve).

Figure 5(b) presents the same quantities as those plotted in Fig. 5(a), but with the Si cylinder vertically moving upwards from the maximum intensity point of the nanojet spatial distribution. The absence or presence of the resonance in this particle is shown by the black
square and green up-triangle curves, respectively. Obviously, due to the symmetry of the field intensity map around this axis, no horizontal force is exerted. In the vertical direction the particle is nevertheless fairly strongly pushed upwards, the force magnitude following an oscillatory behavior due to the interference pattern between the field exiting the slit and that reflected down by the Si cylinder. This push is weak if the WGM resonance is excited. In this latter case, under this p-polarization illumination most of the near field is concentrated inside the particle, with little intensity outside. This leads to such weak optical forces on the resonant particle with the p-polarized WGM in both Figs. 5(a) and 5(b).

It is worth remarking that these forces $F^t_x$ and $F^t_y$ induced by the nanojet on the Si particle are about 1000 and 10 times larger, respectively, than those from direct illumination of this probe cylinder by the Gaussian beam like in a conventional optical tweezer, (compare the above Figs. 5(a) and 5(b) with Figs. 5(a) and 5(b) of [14]).

![Graphs showing X- and Y-components of the optical force](image)

**FIG. 6.** (a) X-component $F^t_x$ of the total electromagnetic force exerted on the Si cylinder placed on the exit of the slit practiced in the Al slab illuminated by a nanojet that arises near the back surface of the SiO$_2$ - glass cylinder of radius $r_{nj} = 3\mu m$ below the slit, See Fig.1. The Si cylinder is tangent to the exit plane of the slit, and laterally moves to the right from the aperture axis. (b) Y-component $F^t_y$ of the optical force when the Si cylinder moves as in (a). In both graphics, black square and red circle curves stand for the cases in which the probe cylinder is non-resonant ($\lambda = 1280nm$) and resonant ($\lambda = 1160nm$), respectively.

On the other hand, Figs. 6(a) and 6(b) show the X- and Y-components of the optical force exerted on the Si cylinder, placed on the exit of the subwavelength slit, by the electromagnetic field exiting it. A SiO$_2$ - glass cylinder of radius $r_{nj} = 3\mu m$ is below the slit and forms a nanojet near its back surface. The particle laterally moves to the right approaching the slit edge. Each force Cartesian component is plotted for the Si cylinder being either out
or in resonance. Now this particle is more and more horizontally attracted by the corners of
the slit exit as it approaches them, independently of the absence or presence of the resonance
[see the black square and red circle curves, respectively, in Fig. 6(a)], the horizontal force
being stronger in resonance. Notwithstanding, the slit exerts a pushing vertical force on the
cylinder which decreases as it moves to the slit corners, [cf. black squared and red circled
curves, respectively, in Fig. 6(b)]. Then, the presence of the resonant $WGM_{2,1}$ in the $Si$
particle causes the vertical push from the slit to decrease and the horizontal attraction to
the slit corners to increase. The cause of this is the same as discussed in connection with
Figs. 5(a) and 5(b) for $p$-polarized illumination. However, as regards the horizontal force
near the slit edge, the gradient force created around this edge by its concentration of charge,
[see Figs. 4(b) and 4(c)], is responsible for the larger value of $F_x$ in resonance near this
edge, as seen in Fig. 6(a). Thus, solely the field intensity gradient near the exit corners of
the slit, (remember that in resonance under $p$-polarization the $Si$ cylinder concentrates the
intensity inside, leaving very little scattered energy in its surroundings), is the major factor
concerning the interaction between the aperture and the resonant particle.

These forces induced by the nanojet on the $Si$ particle through the slit are about 3 and
6 times larger than those from direct illumination of the slit by the Gaussian beam, i.e.
without nanojet, (compare the above Figs. 6(a) and 6(b) with Figs. 5(a) and 5(b) of [14]).

EXTRAORDINARY TRANSMISSION OF A SUBWAVELENGTH SLIT ILLUMI-
NATED BY A NANOJET. EXCITATION OF A LOCALIZED SURFACE PLAS-
MON.

Excitation of a localized surface plasmon in a cylinder by nanojet focalization.

Effects of coupling by supertransmission

We now deal with a subwavelength slit illuminated by a nanojet in the ultraviolet region
when a metallic cylinder is at its exit. This produces two interacting processes of extraor-
dinary transmission, or supertransmission, enhancement: one due to the coupling of the
nanojet focused in the aperture with the excitation of its propagating eigenmodes, and that
arising from the coupling of the field transmitted through the slit with the localized surface
plasmon (LSP) excited on the metallic cylinder, [14, 39]. In order to analyze the optical
force on the metallic particle, we first briefly discuss the distribution of fields and energy in this system.

![Graph](image)

FIG. 7. (a) Time-averaged energy flow norm $|<S(r)>|$ versus illumination wavelength, transmitted at the exit of a slit (width $d = 109.7\text{nm}$) practiced in an Al slab (width $D = 5.096\mu\text{m}$, thickness $h = 219.4\text{nm}$) illuminated by a nanojet. This nanojet is focused by a $\text{SiO}_2 - \text{glass}$ cylinder of radius $r_{nj} = 1.3\mu\text{m}$, $10\text{nm}$ separated from the entrance plane of the slit. (b) No slit is present: $|<S(r)>|$ against illumination wavelength, concentrated on the surface of an Ag cylinder of radius $r = 30\text{nm}$ placed at $200\text{nm}$ from the back surface of the focusing $\text{SiO}_2 - \text{glass}$ cylinder. (c) The same quantity when the slit is present and the Ag cylinder, tangent to the exit plane of the aperture, scatters the light exiting the slit which is illuminated by the nanojet. These calculations are done as explained in Fig. 1.

Now a $\text{SiO}_2 - \text{glass}$ cylinder of radius $r_{nj} = 1.3\mu\text{m}$ is placed below an Al slab and focuses, near its back surface, a nanojet which illuminates the slit. The calculations are done as described in Fig. 1. The rather smooth transmitted intensity with peak at $\lambda = 339.7\text{nm}$ that would be obtained if this slit were illuminated by the Gaussian beam without any nanojet, normalized to the maximum intensity (which was $0.75\text{mW}/\mu\text{m}^2$), becomes, when the nanojet illuminates the slit, an oscillatory line, typical of nanojets, as seen in Fig. 7(a). Nevertheless, this configuration may render a slit-nanojet transmittance enhancement factor.
of about 4. Figure 7(b) represents the effect of light concentration in an Ag cylinder of radius \( r = 30\text{nm} \) placed at 200nm from the back surface of the focusing SiO\(_2\) glass cylinder when the slit is suppressed. The excited \( TM_{2,1} \) eigenmode energy concentrated on the surface of the Ag cylinder is enhanced at \( \lambda = 339.7\text{nm} \) by a factor about 33 due to the presence of the nanojet, [see Fig. 7(b)]. This effect is somewhat similar to that on the above studied Si particle, although now with a much stronger enhancement factor.

On the other hand, when the slit is also present as shown in Fig. 7(c), enhancement factors between 8 and 47 are obtained on excitation of the \( TM_{2,1} \) LSP in the Ag cylinder.

![Image](image.png)

**FIG. 8.** (a) Detail of the electric field spatial distribution \( \mathbf{E}(\mathbf{r}), \mathbf{r} = (x, y) \), (magnitude and vector: colors and arrows, respectively), near the Ag cylinder of radius \( r = 30\text{nm} \) placed at 200nm from the back surface of the focusing SiO\(_2\) glass cylinder of radius \( r_{nj} = 1.3\mu\text{m} \). No slit is present. (b) The same detail but now in time-averaged energy flow \( \langle \mathbf{S}(\mathbf{r}) \rangle \), (norm in colors and vector in arrows). (c) Detail of \( \mathbf{E}(\mathbf{r}) \) (magnitude and vector: colors and arrows, respectively), when the slit is also present. The configuration corresponds to the largest peak in of Fig. 7(c). \( |\mathbf{E}(\mathbf{r})|_{max} = 2.513 \times 10^7 \text{V/m} \). (d) The same detail as in (c), now in \( \langle \mathbf{S}(\mathbf{r}) \rangle \) (norm in colors and vector in arrows). \( |\langle \mathbf{S}(\mathbf{r}) \rangle|_{max} = 9.265 \times 10^{10} \text{W/m}^2 \). In all images the illumination wavelength is \( \lambda = 339.7\text{nm} \).

As illustrations, Figs. 8(a) and 8(b) present details of the effect of the nanojet near the
Ag cylinder. As seen, there is a skin depth effect at the illuminating wavelength due to the small size of this Ag cylinder. This case corresponds to the largest peak in Fig. 7(b). The electric field $\mathbf{E}(\mathbf{r})$ and the time-averaged energy flow $<\mathbf{S}(\mathbf{r})>$, respectively, are also shown. The nanojet is almost completely concentrated in the small metallic cylinder. Figs. 8(c) and 8(d) are details of $\mathbf{E}(\mathbf{r})$ and $<\mathbf{S}(\mathbf{r})>$, respectively, for the configuration studied in Fig. 7(c) i.e. that of the nanojet-LSP coupling through the slit. The wavelength $\lambda = 339.7nm$ corresponds to the largest peak in Fig. 7(c), which practically remains the same as that of Fig. 7(b) when there is no slit. The hotspots in the slit edge, the nanojet focalization as well as the LSP excitation mechanisms are shown.

Electromagnetic forces on a metallic cylinder with a localized surface plasmon excited by a nanojet, either directly or on transmission through a subwavelength slit.

We now are in position to analyze the optical forces induced by the nanojet and the slit on the metallic Ag particle with excitation LSPs.

**FIG. 9.** (a) X- and Y-components of the total electromagnetic force $\mathbf{F}_t^l$, calculated as explained in Fig. 1 and Eq. (1), due to the nanojet focused by the $\text{SiO}_2 – \text{glass}$ cylinder, acting on the Ag cylinder of radius $r = 30nm$ as this laterally moves to the right from the point of maximum intensity of the nanojet. (This point is on the vertical symmetry axis at 200nm from the back surface of the $\text{SiO}_2 – \text{glass}$ cylinder). No slit is present. (b) The same when the Ag cylinder vertically moves upwards from the point of maximum intensity of the nanojet. In both figures, black squared and triangle up green curves stand for $\mathbf{F}_t^x$, both when the Ag cylinder is non-resonant ($\lambda = 500.0nm$) and when it is resonant ($\lambda = 339.7nm$), respectively. Red circle and triangle down blue lines represent $\mathbf{F}_t^y$ in the same order and for the same cases as before.
To this end, the excitation of the Ag cylinder $TM_{2,1}$ LSP eigenmode by focusing a nanojet on it, is studied. Figure 9(a) shows the behavior of the X- and Y-components of the force on this metallic particle as it progressively moves to the right in absence of the slit. This force is due to only the field of the nanojet scattered by the Ag particle. When the particle is not resonant, the forces along the X and Y directions are very weak, of the order of $10^{-2} fN/nm$ and $10^{-1} fN/nm$ for the horizontal force (black curve with squares) and for the vertical force (red curve with circles), respectively. In resonance the horizontal force is still very weak, but the vertical component is strong and attractive. On the other hand, as the Ag cylinder moves upwards along the nanojet axis, as shown in Fig. 9(b), no transversal force appears (black squared and green up-triangled curves, respectively) as it should, but differences in the vertical force arise depending on the absence or the presence of a LSP resonance. This vertical force is very small in absence of LSP excitation: about $10^{-1} fN/nm$, whereas it is attractive and oscillating with distance, and of the order of $10^{3} fN/nm$ when the LSP resonance of the Ag cylinder is excited, this oscillation is due to the interference pattern between the nanojet inciding on the metallic particle and the field that the latter scatters backward.

Notice the remarkable pulling nature of this vertical force, which converts the SiO$_2$-glass cylinder in a photonic tractor [63–65] for certain plasmonic small particles. This contrasts with the repulsive $F_y$ obtained in [48] on an Ag particle in resonance. However, if one doubles its radius making it of 60 nm, then this force becomes repulsive due to its larger scattering cross section. We do not show this here for brevity.

Finally, the presence of the slit illuminated by the nanojet is analyzed concerning the optical forces acting on the Ag cylinder. Once again, the excitation of a LSP resonance largely affects these forces, but due to $p$-polarized illumination, it has consequences opposite to those of the WGM excitation in a dielectric particle, (cf. Figs. 10(a) and 10(b) for the X- and Y-components of this optical force, respectively). Black square and red circle curves in Fig. 10(a) stand for the cases of absence and presence of LSP resonance in the Ag cylinder, respectively. They show that the plasmonic resonance enhances the lateral force, which progressively attracts the particle towards the corners as it approaches it in its displacement. The vertical force, plotted with the same color code in Fig. 10(b), behaves in a more complex way. This being slightly attractive when the Ag cylinder is non resonant (values of order $10^{-1} fN/nm$). However, in presence of resonance this vertical force is,
FIG. 10. (a) X-component $F_t^x$ of the total electromagnetic force exerted on the Ag cylinder of radius $r = 30\,\text{nm}$, calculated as explained in Fig. 1 and Eq. (1). The slit is practiced in the Al slab, being illuminated by the nanojet which arises from the back surface of the $\text{SiO}_2 - \text{glass}$ cylinder placed below. The Ag cylinder is tangent to the exit plane of the slit, and laterally moves to the right from the aperture axis. (b) Y-component $F_t^y$ of the optical force when the Ag cylinder moves as in (a). In both graphics, black square and red circle curves stand for the cases in which the Ag cylinder, tangent to the exit line of the aperture, is non-resonant ($\lambda = 1280\,\text{nm}$) and resonant ($\lambda = 1160\,\text{nm}$), respectively. The green up triangles and blue down triangles curves represent, in the same order as before, the same cases when the Ag cylinder is at the exit slit, 20nm inwards.

Though, repulsive in the central region of the slit exit, becoming attractive near its corners (red circled curve). These tendencies can be increased by locating the Ag cylinder inwards the slit exit, as noticed by the green up-triangles and blue down-triangles curves of both Figs. 10(a) and 10(b). [Values of order $10^{-1}\,\text{fN/nm}$ for the green up triangles curve (non resonant cylinder) in Fig. 10(b)].

In any case, the forces induced by the nanojet on the Ag particle through the slit are about 10 times larger than those from direct illumination of the slit by the Gaussian beam without nanojet, (compare the above Figs. 10(a) and 10(b) with Figs. 11(a) and 11(b) of [14]).

DISCUSSION AND CONCLUSIONS

We have made a study on the photonic forces on nanoparticles near a subwavelength slit illuminated by a nanojet. We have performed comparisons of the force on the particles either in or out of their Mie resonance excitation. The study has been done in 2D, so that
these objects are cylinders and the transmission modes of the slit are excited by p-polarized illumination. However, we believe that these results also hold for spheres in 3D, aside of polarization effects.

We have proven that whereas the morphological resonance of the slit, causing supertransmission, enhances the fields surrounding the probe cylinders and hence the optical forces exerted upon them, the excitation of the probe particle resonance has a different effect on these forces, according to whether the cylinder is dielectric or metallic.

The photonic force on the probe particle depends on the field surrounding it. Thus WGMs in dielectric nanocylinders under p-polarization, (which is the one at which supertransmission exists in 2D), have no much effects on the optical force. Its strength may weaken due to the low intensity distribution in the near field region of this particle. In this connection, it must be remarked that the electromagnetic force on dielectric cylinders is however enhanced under s-polarization illumination \[50\]; then the WGM extends to the near field outside the cylinder.

On the other hand, LSPs in metallic nanocylinders give rise to localized field energy enhancement on the cylinder surface; this strengthens the optical force. In contrast with illumination by only a PNJ, the presence of a subwavelength slit enriches the effect of the electromagnetic forces. Whereas such a a small metallic particle resonantly illuminated by a nanojet, suffers an attractive vertical force which makes the $SiO_2 - glass$ nanojet forming cylinder to behave as a photonic tractor, the additional presence of a subwavelength aperture may change the sign of this force thus transforming it to repulsive, depending on the lateral position of the cylinder.

For any cylinder, whether dielectric or metallic, we observe that illuminating the slit with a nanojet increases the magnitude of the optical forces on the particle by a factor between 3 and 10 compared with illumination of the slit with a Gaussian beam. On the other hand, the gradient horizontal force induced by a nanojet in a dielectric particle is a few orders of magnitude larger than that of a Gaussian beam of a conventional optical tweezer.

These results should stimulate experiments with PNJs on slits since they are the result of focusing by microparticles, and their highly localized intensity at the subwavelength scale present an ideal means to spatially control the mechanical action on nanoobjects.
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