Gated Recurrent Context: Softmax-free attention for Online Encoder-Decoder Speech Recognition

Hyeonseung Lee, Woo Hyun Kang, Sung Jun Cheon, Hyeongju Kim, and Nam Soo Kim, Senior Member, IEEE

Recently, attention-based encoder-decoder (AED) models have shown state-of-the-art performance in automatic speech recognition (ASR). As the original AED models with global attentions are not capable of online inference, various online attention schemes have been developed to reduce ASR latency for better user experience. However, a common limitation of the conventional softmax-based online attention approaches is that they introduce an additional hyperparameter related to the length of the attention window, requiring multiple trials of model training for tuning the hyperparameter. In order to deal with this problem, we propose a novel softmax-free attention method and its modified formulation for online attention, which does not need any additional hyperparameter at the training phase. Through a number of ASR experiments, we demonstrate the tradeoff between the latency and performance of the proposed online attention technique can be controlled by merely adjusting a threshold at the test phase. Furthermore, the proposed methods showed competitive performance to the conventional global and online attentions in terms of word-error-rates (WERs).

Index Terms—Automatic Speech Recognition, Online speech recognition, Attention-based encoder-decoder model

I. INTRODUCTION

In the last few years, the performance of deep learning-based end-to-end automatic speech recognition (ASR) systems has improved significantly through numerous studies mostly on the architecture designs and training schemes of neural networks (NNs). Among many end-to-end ASR systems, attention-based encoder-decoder (AED) models [1], [2] have shown better performance than the others, such as the connectionist temporal classification (CTC) [3] and recurrent neural network transducer (RNN-T) [4], and even outperformed the conventional DNN-hidden Markov model (HMM) hybrid systems in case a large training set of transcribed speech is available [5]. Such successful results of AED models come from the tightly integrated language modeling capability of the label-synchronous decoder, supported by the attention mechanism that provides proper acoustic information at each step [6].

A major drawback of the conventional AED models is that they cannot infer the ASR output in an online fashion, which degrades the user experience due to the large latency [7]. This problem is mainly caused by the following aspects of the AED models. Firstly, the encoders of most high-performance AED models make use of layers with global receptive fields, such as bidirectional long short-term memory (BiLSTM) or self-attention layer. More importantly, a conventional global attention mechanism (e.g., Bahdanau attention) considers the entire utterance to obtain the attention context vector at every step. The former issue can be solved by replacing the global-receptive encoder with an online encoder, where an encoded representation for a particular frame depends on only a limited number of future frames. The online encoder can be built straightforwardly by employing layers with finite future receptive field such as latency-controlled BiLSTM (LC-BiLSTM) [8] and masked self-attention layers. However, reformulating the global attention methods for an online purpose is still a challenging problem.

Conventional techniques for online attention are usually two-step approaches where the window (i.e., chunk) for the current attention is determined first at each decoder step, then the attention weights are calculated using the softmax function defined over the window. As the softmax function is a common solution for representing discrete probability distributions (i.e., attention weights), existing online attentions mainly differ in how they determine the window. Neural transducers [9], [10] divide an encoded sequence into multiple chunks with a fixed length, and the attention-decoder produces an output sequence for each input chunk. In the windowed attention techniques [11], [12], [13], the position of each fixed-size window is decided by a position prediction algorithm. The window position is monotonically increasing in time, and some approaches employ a trainable position prediction model with a fixed Gaussian window. In MoChA-based approaches [14], [15], [16], a fixed-size chunk is obtained using a monotonic endpoint prediction model, which is jointly trained considering all possible chunk endpoints.

A common limitation of the aforementioned approaches is that the fixed-length of the window needs to be tuned according to the training data. Merely choosing a large window of a constant size causes a large latency while setting the window size too small results in degraded performance. Therefore multiple trials of the model training are required to find a proper value of the window length, consuming excessive computational resources. Moreover, the trained model does not guarantee to perform well on an unseen test set, since the window size is fixed for all datasets.

Although a few variants of MoChA utilize an adaptive window length to remove the need for tuning the window size, such variants induce other problems. MATChA [14]...
regards the previous endpoint as the beginning of the current chunk. Occasionally, the window can be too short to contain enough speech content when two consecutive endpoints are too close, which may degrade the performance. AMoChA [17] employs an auxiliary model that predicts the chunk size but also introduces an additional loss term for the prediction model. As the coefficient for the new loss needs tuning, AMoChA still requires repeated training sessions. Besides, several recent approaches [18], [19] utilize strictly monotonic windows. But these methods have a limitation in that the decoder state is not used for determining the window, which means such algorithms might not fully exploit the advantage of AED models, i.e., the inherent capability of autoregressive language modeling.

The aforementioned inefficiency in training the conventional online attentions is essentially caused by the fact that the softmax function needs a predetermined attention window to obtain the attention weights, which results in repetitive tuning process of the window-related hyperparameter. To overcome this drawback, we propose a novel softmax-free global attention method called gated recurrent context (GRC), inspired by the gate-based update in gated recurrent unit (GRU) [20]. Whereas conventional attentions are based on a kernel smoother (e.g. softmax function) [21], [22], GRC obtains an attention context vector by recursively aggregating the encoded vectors in a time-synchronous manner, using update gates. GRC can be reformulated for the purpose of online attention, which we refer to decreasing GRC (DecGRC), where the update gates are constrained to be decreasing over time. DecGRC is capable of deciding the attention-endpoint by thresholding the update gate values at the inference phase. DecGRC as well as GRC introduces no hyperparameter to be tuned at the training phase. The main contributions of this paper can be summarized as follows:

- We propose a novel softmax-free attention method called **Gated Recurrent Context (GRC).** To the best of our knowledge, GRC is the first attention method that represents discrete probability distributions without a kernel smoother.
- We present a novel online attention method, Decreasing **GRC (DecGRC) ,** a constrained variant of GRC. DecGRC does not need any new hyperparameter to be tuned at the training phase. At test time, the tradeoff between performance and latency can be adjusted using a simple thresholding technique.
- We experimentally show that GRC and DecGRC perform competitive to the conventional global and online attention methods on the LibriSpeech test set.

The remainder of this paper is organized as follows. In Section II the general framework of attention-based encoder-decoder ASR is formally described, followed by conventional online attention methods and their common limitation. Section III proposes formulations of both GRC and DecGRC and the algorithm for online inference. The experimental results with various attention methods are given in Section IV. Conclusions are presented in Section V.
where $\theta$ denotes the set of all trainable parameters, and $|y|$ is the text sequence length of the sampled data. Inference can be performed by searching the most likely text sequence:

$$\hat{y} = \arg\max_{y} \log P(y|x; \theta).$$

**B. Online Attention**

To achieve online attention, the context vector $c_u$ in Eq. (2) must have local dependency on the encoded vectors $h$. Windowed attention and MoChA are widely-used online attention methods that show high performance for which only the AttentionContext($\cdot$) function in Eq. (1) is modified in the general framework.

1) Windowed attention

Among various formulations of windowed attention, a simple heuristic using $\arg\max$ for window boundary prediction [13] has shown the best performance. This method can be described as follows:

$$p_1 = 0, \quad p_u = \arg\max_{t} (\alpha_{u-1,1} \leq t \leq T), \quad \text{Eq. (5)}$$

$$c_u = \sum_{t=p_u}^{p_u+w-1} \alpha_{u,t} h_t, \quad \text{Eq. (6)}$$

$$\alpha_{u,t} = \frac{\exp(e_{u,t})}{\sum_{j=p_u}^{p_u+w-1} \exp(e_{u,j})}, \quad \text{Eq. (7)}$$

where $p_u$ is the start point of the attention window at the $u$-th step, and $w$ is the window size. The windowed attention is online, as the attention context $c_u$ derived through Eqs. (5)-(7) does not depend on the entire encoded vector sequence $h$. The tradeoff between performance and latency of windowed attention relies on the window length $w$.

2) MoChA

In MoChA [14], an attention window endpoint is first decided, followed by attention weights calculation within a fixed-size window as follows:

$$c_u = \sum_{t=\tau_{u-w+1}}^{\tau_{u}} \beta_{u,t} h_t, \quad \text{Eq. (7)}$$

$$\beta_{u,t} = \frac{\exp(e_{u,t})}{\sum_{j=\tau_{u-w+1}}^{\tau_{u}} \exp(e_{u,j})}, \quad \text{Eq. (8)}$$

$$\tau_u = \text{MonotonicEndpoint}(\tilde{e}_{u,\geq \tau_{u-1}}), \quad \text{Eq. (9)}$$

$$\tilde{e}_{u,t} = \text{MonotonicScore}(s_{u,t} h_t, \alpha_{<u,t}) + b \quad \text{Eq. (10)}$$

where MonotonicScore($\cdot$) is a similarity function, $b$ is a trainable bias parameter, $\tilde{e}_{u,t}$ is the monotonic score, and MonotonicEndpoint($\cdot$) is an window end-decision algorithm based on thresholding, and $\beta_{u,t}$ is an attention weight within the window. Note that Eqs. (7)-(10) are substitutes for Eqs. (2)-(6) in GSA. The performance and latency of MoChA are also known to depend on the chunk size $w$.

Optimizing an AED model using these formulations is infeasible since they do not fit the backpropagation framework. To solve this problem, an expectation-based formulation is exploited for training [14]:

$$\beta_{u,t} = \sum_{k=t}^{t+w-1} \frac{\alpha_{u,k} \exp(e_{u,k})}{\sum_{l=k-w+1}^{k} \exp(e_{u,l})}, \quad \text{Eq. (11)}$$

$$\alpha_{u,t} = p_{u,t} \left(1 - p_{u,t-1}\frac{\alpha_{u,t-1}}{p_{u,t-1}} + \alpha_{u-1,t}\right), \quad \text{Eq. (12)}$$

$$p_{u,t} = \sigma(e_{u,t})$$

where $p_{u,t}$ is a stopping probability at the $t$-th time step and $\alpha_{u,t}$ is an accumulated selection probability that the window endpoint is $t$.

3) Limitation of the conventional methods

As mentioned in Sec. I, the softmax function in the conventional online attentions (e.g., Eqs. (6)-(8)) requires a predetermined attention window, which induces a limitation in training efficiency since multiple trials of training are inevitable for tuning either the window length or the coefficient of an additional loss term. To overcome this limitation, in the next section, we propose a novel softmax-free global attention method and its online version which is free from the tuning of hyperparameters in training.

**III. PROPOSED METHODS**

**A. Gated Recurrent Context (GRC)**

We propose a novel softmax-free global attention method called GRC, which recursively aggregates the information of the encoded sequence into an attention context vector in a time-synchronous manner. Specifically, the following formulas are employed in place of the Eqs. (2)-(6):

$$c_u = d_{u,T}, \quad \text{Eq. (11)}$$

$$d_{u,t} = (1 - z_{u,t}) d_{u,t-1} + z_{u,t} h_t, \quad \text{Eq. (12)}$$

$$z_{u,1} = 1, \quad z_{u,t} = \sigma(e_{u,t}) = \frac{1}{1 + \exp(e_{u,t})}, \quad \text{Eq. (13)}$$

$$c_{u,t} = \text{Score}(s_{u,t} h_t, \alpha_{<u,t}) + b \quad \text{Eq. (14)}$$

where $z_{u,t}$ and $d_{u,t}$ are the update gate and the intermediate attention context vector for the $t$-th time step at the $u$-th decoder step, respectively. GRC computes an intermediate value for the final context vector recursively in time, inspired by GRU [20]. Note that Eqs. (11)-(14) of GRC do not utilize the softmax function at all, unlike the conventional attentions. Nevertheless, GRC can be interpreted as a global attention method, since it calculates a weighted average of the encoded sequence over the whole time period, as explained in Sec. III-AT.

1) Relation to GSA

The update gate $z_{u,t}$ of GRC in Eq. (13) and the attention weight $\alpha_{u,t}$ of GSA in Eq. (3) have one-to-one correspondence according to the following theorem:

**Theorem 1** (GRC-GSA duality). For arbitrary $n \in \mathbb{N}$, let $Z^n = \{x \in \mathbb{R}^n | x_1 = 1, 0 \leq x_j \leq 1 \text{ for } j = 2, 3, \ldots, n\}$ and $A^n = \{x \in \mathbb{R}^n | \sum_{j=1}^{n} x_j = 1, 0 \leq x_j \leq 1 \text{ for } j = 1, 2, \ldots, n\}$. There exists a bijective function $\hat{\alpha} : Z^n \rightarrow A^n$ s.t.
for any \( h = [h_1, h_2, \ldots, h_T] \) and \( z_u = [z_{u,1}, z_{u,2}, \ldots, z_{u,T}] \), the following holds:

\[
d_{u,T} = \sum_{t=1}^{T} \tilde{\alpha}(z_u)_t h_t
\]

where \( \tilde{\alpha}(z_u)_t \) denotes the \( t \)-th element of \( \tilde{\alpha}(z_u) \), and \( d_{u,T} \) is obtained from \( z_u \) and \( h \) according to Eq. (12).

**Proof.** Using the recursive Eq. (12),

\[
d_{u,T} = (1 - z_{u,T})d_{u,T-1} + z_{u,T} h_T = (1 - z_{u,T})d_{u,T-2} + (1 - z_{u,T})h_T - 1 + z_{u,T} h_T = \ldots
\]

\[
= \sum_{t=1}^{T} \left( \prod_{j=t+1}^{T} (1 - z_{u,j}) \right) z_{u,T} h_T.
\]

Therefore the function \( \tilde{\alpha} \) that satisfies Eq. (1) is given by

\[
\tilde{\alpha}(z_u)_t := z_{u,t} \prod_{j=t+1}^{T} (1 - z_{u,j}) \quad \text{for } t = 1, 2, \ldots, T. \quad (15)
\]

Given that \( z_u \in \mathbb{Z}^T \), the output \( \tilde{\alpha}(z_u) \) is an element of \( A^T \) because it is trivial to show that \( 0 \leq \tilde{\alpha}(z_u)_t \leq 1 \) for \( i = 1, 2, \ldots, T \), and also \( \sum_{t=1}^{T} \tilde{\alpha}(z_u)_t = 1 \) holds as follows:

\[
\sum_{t=1}^{T} \tilde{\alpha}(z_u)_t = \sum_{t=1}^{T} z_{u,t} \prod_{j=t+1}^{T} (1 - z_{u,j}) = \sum_{t=2}^{T} z_{u,t} \prod_{j=t+1}^{T} (1 - z_{u,j}) + \prod_{j=2}^{T} (1 - z_{u,j})
\]

\[
= \sum_{t=3}^{T} z_{u,t} \prod_{j=t+1}^{T} (1 - z_{u,j}) + \prod_{j=3}^{T} (1 - z_{u,j}) = \ldots = z_{u,T} + (1 - z_{u,T}) = 1.
\]

The \( \tilde{\alpha}(z_u) \) is a bijective function since the inverse mapping of \( \tilde{\alpha} \) exists as follows:

\[
z_{u,T} = \tilde{\alpha}(z_u)_T,
\]

\[
z_{u,T-1} = \begin{cases} \tilde{\alpha}(z_u)_{T-1} - \tilde{\alpha}(z_u)_{T-1} \quad & \text{if } \tilde{\alpha}(z_u)_T < 1; \\ 0 & \text{otherwise}, \end{cases}
\]

\[
z_{u,T-2} = \begin{cases} \tilde{\alpha}(z_u)_{T-2} - \tilde{\alpha}(z_u)_{T-2} \quad & \text{if } \sum_{j=T-1}^{T} \tilde{\alpha}(z_u)_j < 1; \\ 0 & \text{otherwise}, \end{cases}
\]

\[
\vdots
\]

\[
\vdots z_{u,t} = \begin{cases} \tilde{\alpha}(z_u)_t - \sum_{j=t+1}^{T} \tilde{\alpha}(z_u)_j \quad & \text{if } \sum_{j=t+1}^{T} \tilde{\alpha}(z_u)_j < 1; \\ 0 & \text{otherwise}, \end{cases}
\]

for \( t = 1, 2, \ldots, T \). It is also trivial to show that \( z_{u,1} = 1 \) and \( 0 \leq z_{u,t} \leq 1 \) for \( i = 2, \ldots, T \), given that \( \tilde{\alpha}(z_u) \in A^T \).

Therefore, \( z_u \in \mathbb{Z}^T \).

Note that \( \tilde{\alpha}(z_u)_t \) in Eq. (15) corresponds to the attention weight \( \alpha_{u,t} \) in Eq. (3) of GSA. By Thm. [1] the attention context vector \( c_u \) of GRC is capable of expressing all possible weighted averages of the encoded representations over time, as in the GSA. Thus the range of \( c_u \) in GRC or GSA is the same. Nonetheless, we empirically showed that GRC performs comparable to or even better than GSA, and the experimental results are given in Sec. [IV]

2) Relation to sMoChA

The sMoChA \([15]\) is a variant of MoChA where Eq. (10) is replaced by the following formula:

\[
\alpha_{u,t} = p_{u,t} \prod_{j=1}^{t-1} (1 - p_{u,j}) \quad (16)
\]

which enables the optimization process to be more stabilized. Eq. (16) is almost similar to the function \( \tilde{\alpha} \) in Eq. (15), and implies evidence on the stability of GRC training. Despite this fact, sMoChA is an algorithm independent of GRC, as Eq. (16) is merely used as the selection probability component in the whole training formulas and not even used for inference.

### B. Decreasing GRC (DecGRC)

The intermediate context \( d_{u,t} \) of GRC is a weighted average of the encoded representations over time according to the following corollary:

**Corollary 1.1** (Weighted average). Let \( Z^n \) and \( A^n \) be the sets defined in Thm. [2]. For any \( \tau \in \{1, 2, \ldots, T\} \), \( z_u \in Z^T \), and \( h = [h_1, h_2, \ldots, h_T] \), there exists a function \( \bar{\alpha} : Z^T \rightarrow A^T \) that satisfies the following equation:

\[
d_{u,\tau} = \sum_{t=1}^{T} \bar{\alpha}(z_u)_t h_t
\]

where \( \bar{\alpha}(z_u)_t \) denotes the \( t \)-th element of \( \bar{\alpha}(z_u) \), and \( d_{u,\tau} \) is obtained from \( z_u \) and \( h \) according to Eq. (17).

**Proof.** By substituting every \( T \) in the proof of Thm. [1] with \( \tau \), there exists a bijective function \( \bar{\alpha} : Z^\tau \rightarrow A^\tau \) given by

\[
\bar{\alpha}(z_u)_t := z_{u,t} \prod_{j=t+1}^{\tau} (1 - z_{u,j}) \quad \text{for } t = 1, 2, \ldots, \tau,
\]

such that

\[
d_{u,\tau} = \sum_{t=1}^{\tau} \bar{\alpha}(z_u)_t h_t.
\]

It is trivial to show that the following function \( \bar{\alpha} : Z^\tau \rightarrow A^\tau \) satisfies the equation in Coroll. [11]:

\[
\bar{\alpha}(z_u)_t = \begin{cases} \bar{\alpha}(z_u)_t & \text{if } t \leq \tau; \\ 0 & \text{otherwise}, \end{cases} \quad \text{for } t = 1, 2, \ldots, T.
\]

Global attention methods including GSA and GRC cannot compute the attention weights without the entire sequence of the encoded vectors \( h \). However, considering that the attention techniques are methods for calculating the weighted average of the encoded vectors, Coroll. [11] enables us to treat an
Algorithm 1 Online inference using DecGRC.

\begin{algorithm}
\begin{algorithmic}
  \State \textbf{Input:} encoded vectors $h$ of length $T$, threshold $\nu$
  \State \textbf{State:} $s_0 = 0$, $u = 1$, $y_0 = \text{StartOfSequence}$
  \While{$y_{u-1} = \text{EndOfSequence}$}
    \State $d_u = h_1$
    \For{$t = 2$ to $T$}
      \State $e_{u,t} = \text{Score}(s_u, h_t, \alpha_{u,t}) + b$
      \State $z_{u,t} = 1/(1 + \sum_{j=1}^{t} \exp(e_{u,j}))$
      \State $d_u = (1 - z_{u,t})d_u + z_{u,t}h_t$
      \If{$z_{u,t} < \nu$}
        \State break
      \EndIf
      \State $s_u = \text{RecurrentState}(s_{u-1}, y_{u-1}, d_u)$
      \State $\hat{P}(y_u|y_{<u}, h) = \text{ReadOut}(s_u, y_{u-1}, c_u) // \text{softmax}$
      \State $y_u = \text{Decide}(\hat{P}(y_u|y_{<u}, h)) // \text{choose a text unit in the vocabulary. (e.g. argmax for greedy search)}$
      \State $u = u + 1$
    \EndFor
  \EndWhile
\end{algorithmic}
\end{algorithm}

intermediate context $d_{u,t}$ as a substitute for the attention context vector $c_u$ in Eq. (11) of GRC even when the whole encoded sequence is not provided.

Inspired by this, we further propose a novel online attention algorithm, namely DecGRC. DecGRC is a modified version of GRC, replacing Eq. (13) with

\begin{equation}
  z_{u,1} = 1, \quad z_{u,t} = \frac{1}{1 + \sum_{j=1}^{t} \exp(e_{u,j})}.
\end{equation}

Note that the update gate is constrained to be monotonically decreasing over time. Assume that there exists an endpoint index $t_{\text{end}}$ with which $z_{u,t_{\text{end}}}$ has a very small value (e.g. less than 0.001). Considering that $z_{u,t} < z_{u,t_{\text{end}}}$ holds for all $t > t_{\text{end}}$, the difference between $d_{u,t_{\text{end}}}$ and $d_{u,T}$ is small, as the numerical change $|d_{u,t_{\text{end}}} - d_{u,T}|$ for $t > t_{\text{end}}$ induced by the recursion rule in Eq. (12) is negligible if $z_{u,t_{\text{end}}}$ is small enough. Intuitively, intermediate context vectors roughly converge after the endpoint.

DecGRC can operate as an online attention method if such an endpoint index $t_{\text{end}}$ exists at each decoder step and the index can be decided by the model. We experimentally observed that DecGRC models adequately learn the alignment between encoded vectors and text output units, and the intermediate context nearly converges after the aligned time index at each decoder step. Relevant experimental results are given in Sec. IV-D.

Accordingly, with an online encoder, online inference can be implemented via a well-trained DecGRC model. We describe the online inference technique in Alg. 1 where the endpoint index is decided simply by thresholding the update gate values.

C. Computational efficiency of proposed methods

GRC or DecGRC increases negligible amount of memory footprint, since only one trainable parameter $b$ in Eq. (14) is added to the standard GSA-based AED model.

Both proposed methods have computational complexity of \(O(TU)\), same as the conventional global attentions. However, in practice, a speech sequence is linearly aligned with the text sequence on average. As Alg. 1 only regards to encoded vectors before endpoint indices, the total number of steps in the for loop is typically slightly larger than \(TU/2\), if the threshold \(\nu\) is set to an appropriate value. Therefore, DecGRC is computationally more efficient than the global attentions such as GRC and GSA.

The recursive updating in Eq. (12) induces negligible amount of computation compared to the whole training or inference process. There still exists a room for faster computation by enabling parallel computation in time. The parallel computation can be implemented by utilizing Eq. (12) where \(\alpha(z_u)\) is replaced with \(\tilde{\alpha}(z_u)\) in Eq. (15), instead of Eqs. (11)- (12).

Most importantly, both proposed methods introduce no hyperparameter at the training phase. Thus the proposed methods do not need to repeat training to find a proper value of such a hyperparameter. Though the DecGRC inference in Alg. 1 introduces a new hyperparameter (i.e., threshold \(\nu\)) at test phase, the threshold searching on development sets does not take a long time, because the size of the development sets are minor compared to the training set. Hence the total time spent to prepare an ASR system can be saved. Furthermore, the tradeoff between latency and performance can be adjusted by resetting the threshold value \(\nu\) at inference phase, unlike the conventional online attention methods [9], [13], [14]. In these existing methods, the inference algorithms’ decision rules on the attention endpoints are determined at the training phase, and remains unchanged at the test stage. The experiments on DecGRC with different thresholds are demonstrated in Sec. IV-E.

IV. EXPERIMENTS

A. Configurations

All experiments were conducted on LibriSpeech dataset\(^1\), which contains 16 kHz read English speech with transcription. The dataset consists of 960 hours of a training set from 2,338 speakers, 10.8 hours of a dev set from 80 speakers, and 10.4 hours of a test set from 66 speakers, with no overlapping speakers between different sets. Both dev and test sets are split in half into clean and other subsets, depending upon the ASR difficulty of each speaker. We randomly chose 1,500 utterances from dev set as a validation set.

All experiments\(^2\) shared the same network architecture and training scheme of a recipe of RETURNN toolkit\([24],[25]\), except the attention methods. Input features were 40-dimensional mel-frequency cepstral coefficients (MFCCs) extracted with Hanning window of 25 ms length and 10 ms hop size, followed by global mean-variance normalization. Output text units were 10,025 byte-pair encoding (BPE) units extracted from transcription of LibriSpeech training set. The Encoder(·) consisted of 6 BiLSTM layers of 1,024 units for

\(1\) The LibriSpeech dataset can be downloaded from [http://www.openslr.org/](http://www.openslr.org/)

\(2\) The scripts for all experiments are available at [https://github.com/GRC-anonymous/GRC](https://github.com/GRC-anonymous/GRC)
TABLE I
WORD ERROR RATES (WERs) COMPARISON BETWEEN ATTENTION METHODS ON LIBRISPEECH DATASET.

| EXP. ID | ATTENTION METHOD | PARAM. INIT. FROM | IS ATTENTION ONLINE? | IS ENCODER ONLINE? | CAN INFER ONLINE? | WER [%] |
|---------|------------------|-------------------|---------------------|--------------------|-------------------|---------|
|         |                  |                   |                     |                    |                   | CLEAN   | OTHER | CLEAN | OTHER |
| E1      | GSA (Bbahdanau)  | -                 | No                  | No                 | No (BILSTM)       | 14.11   | 9.42  | 15.15 | 14.59 |
| E2      | GRC              | -                 | No                  | No                 |                  | 14.06   | 8.88  | 14.59 |       |
| E3      | WINDOWED ATT. (w=11) | E1             | Yes                 | No                 |                  | 14.82   | 7.51  | 15.90 | 14.98 |
| E4      | WINDOWED ATT. (w=20) | E1             | Yes                 | No                 |                  | 15.11   | 8.17  | 16.18 |       |
| E5      | MoChA (w=2)     | -                 | No                  | No                 |                  | 14.20   | 4.95  | 15.32 |       |
| E6      | MoChA (w=8)     | -                 | No                  | No                 |                  | 14.59   | 5.10  | 15.85 |       |
| E7      | DecGRC (ν=0.01) | E2                | Yes                 | Yes                | (LC-BILSTM)      | 14.10   | 4.83  | 14.90 |       |
| E8      | DecGRC (ν=0.08) | E12               | Yes                 | Yes                | (LC-BILSTM)      | 15.14   | 6.18  | 16.97 |       |
| E9      | GSA (Bbahdanau)  | -                 | No                  | No                 |                  | 14.49   | 5.51  | 16.91 |       |
| E10     | GRC              | E1                | No                  | No                 |                  | 14.44   | 5.17  | 16.40 |       |
| E11     | GRC              | -                 | No                  | No                 |                  | 14.05   | 5.55  | 15.88 |       |
| E12     | GRC              | E2                | Yes                 | Yes                | (LC-BILSTM)      | 15.14   | 6.18  | 16.97 |       |
| E13     | WINDOWED ATT. (w=11) | E10            | Yes                 | Yes                | (LC-BILSTM)      | 14.10   | 4.83  | 14.90 |       |
| E14     | WINDOWED ATT. (w=20) | E10            | Yes                 | Yes                | (LC-BILSTM)      | 14.10   | 4.83  | 14.90 |       |
| E15     | MoChA (w=2)     | E3                | Yes                 | Yes                | (LC-BILSTM)      | 14.10   | 4.83  | 14.90 |       |
| E16     | MoChA (w=8)     | E6                | Yes                 | Yes                | (LC-BILSTM)      | 14.10   | 4.83  | 14.90 |       |
| E17     | DecGRC (ν=0.01) | E8                | Yes                 | Yes                | (LC-BILSTM)      | 15.14   | 6.18  | 16.97 |       |
| E18     | DecGRC (ν=0.08) | E12               | Yes                 | Yes                | (LC-BILSTM)      | 15.14   | 6.18  | 16.97 |       |

In each direction, and max-pooling layers of stride 3 and 2 were applied after the first two BiLSTM layers respectively. For the online Encoder(·), 6 LC-BiLSTM layers were employed in place of the BiLSTM layers, where the future context sizes were set to 36, 12, 6, 6, 6, and 6 for each layer from bottom to top and the chunk sizes were twice the future context sizes. Both Score(·) and MonotonicScore(·) functions were implemented using Bahdanau score with fertility-based weight feedback and 1,024-dimensional attention key, as in [26]. RecurrentState(·) was implemented with an unidirectional LSTM layer with 1,000 units. ReadOut(·) consisted of a max-out layer with 2×500 units, followed by a softmax output layer with 10,025 units. Weight parameters were initialized with Glorot uniform method [27], and biases were initially set to zero. Optimization techniques were utilized during the training: teacher forcing, Adam optimizer, learning rate scheduling, curriculum learning, and the layer-wise pre-training scheme. Briefly, the models were trained for 13.5 epochs using a learning rate of $8 \times 10^{-4}$ with a linear warm-up starting from $3 \times 10^{-4}$ and the Newbob decay rule [28]. Only the first two layers of Encoder(·) with half-width were used at the beginning of a training, then the width and the number of layers gradually increased to the original size at 1.5 epoch. The CTC multi-task learning [29] with a lambda of 0.5 was employed to stabilize the learning, where CTC loss is measured with another 10,025-units softmax layer on the top of Encoder(·). For the models which began the learning from parameters of a pre-trained model, the layer-wise pre-training was skipped. Every model was regularized by applying dropout rate 0.3 to Encoder(·) layers and the softmax layer and employing label smoothing of 0.1. For each epoch of the training, both cross-entropy (CE) losses and output error rates were measured 20 times on the validation set with teacher forcing. During the inference phase, model with the lowest WER on the dev-other set among all checkpoints was selected as the final model, and performed beam search once on the dev and test sets with a beam size of 12.

We trained MoChA models for 17.5 epochs with five times longer layer-wise pre-training to make them converge. A small learning rate of $10^{-5}$ was used for training windowed attention models as in [13]. Though the numbers of total epochs for different experiments were not the same, each model was optimized to converge and showed negligible improvements after that.

B. Performance comparison between attentions

All experimental results are summarized in Tbl. I. For each experiment, we performed two trials of training with the same configuration and chose a model with the lowest word-error-rate (WER), a word-level Levenshtein distance divided by the number of ground-truth words, on dev-other set.

In E1 to E2 and E9 to E12, GRC showed better performance than the other attention methods on test-other set, showing 3.7% and 3.2% relative error-reduction rate (RERR) compared to GSA when evaluated on BiLSTM and LC-BiLSTM encoder, respectively.

In E3 to E6 and E13 to E16, performances of the conventional online attentions, i.e., windowed attention and MoChA, were shown to be highly dependent on a choice of window size hyperparameter $w$. On the other hand, DecGRC is trained without any additional hyperparameter and only involves a threshold $\nu$ at the inference phase.

In E3 to E8 and E13 to E18, DecGRC outperformed the conventional online attention techniques on BiLSTM encoder. With LC-BiLSTM encoder, the performance of DecGRC on test-other set surpassed the conventional attentions including GSA, while the scores on test-clean set were worse than the competitors. The overall performance of GRC and DecGRC...
is degraded on LC-BiLSTM compared to their preferable performance on BiLSTM, which was conjectured to be caused by the following aspect of the proposed methods; $\bar{\alpha}(z_u)$ in Eq. (15) has a dependency on update-gate values of the future time-steps. Therefore using a short future receptive field of LC-BiLSTM may affect the degradation.

C. Optimization speed

The cross-entropy loss curves on training and dev set in E1, E2, E6, and E7 are depicted in Fig. 1. The model based on each attention method was trained from scratch until convergence, with a few spikes in its training loss curve. A spike in the loss curve occurs when the layer-wise pre-training algorithm inserts a new layer and units into the encoder, as the untrained new components make the performance worse right after the insertion.

GRC converged later than GSA, and DecGRC converged slightly later than GRC. MoChA showed the slowest optimization speed, which was partly due to the 5 times longer layer-wise pre-training scheduling than the others. Such long pre-training was employed to stabilize the training of MoChA, whereas the both GRC and DecGRC successfully converged with the standard pre-training. Note that the longer pre-training of MoChA was adopted because it had failed to converge with a short pre-training in our initial experiments. The relatively stable learning of the proposed methods over MoChA can be explained in relation to sMoChA, as described in Sec. III-A2; the sMoChA stabilized the training of MoChA by utilizing a modified selection probability formula, which is actually almost similar to the attention weight $\bar{\alpha}(z_u)$ of GRC in Eq. (15).

D. Attention analysis

GRC and DecGRC accurately learned alignments between encoded representations and output text units, as illustrated in Fig. 2. An interesting characteristic of GRC was observed that it tended to put much weight on the latter time indices of attention weights, compared to GSA. This can be regarded as an innate behavior of GRC, as the attention weight $\bar{\alpha}(z_u)$ in Thm. 1 is designed to weigh the latter indices when the update gates $z_u,t$ have similar value over several consecutive time-indices. The latter-time-weighing attribute could be especially effective for a long text unit (e.g., a BPE unit "swinging" in Fig. 2), as a long BPE unit often ends with a suffix that might be crucial to distinguish words (e.g., "-ing", "-n’t", or "-est" in English). A piece of statistical evidence is presented in Fig. 3; GRC outperformed GSA when the median length of BPE was larger than or equal to 6, while it showed similar performance for shorter median lengths.

Attention weights of DecGRC tended to be much smoother (i.e., focused on longer time) than GRC and GSA. Such smoothness was hypothesized to be caused by the decreasing...
update gates, which made the model trained to be cautious for a sharp descent of update gate values, as it is irreversible in DecGRC. In addition, DecGRC did not attend on the first time index, unlike GSA and GRC. It is an intrinsic property of DecGRC, as the earliest update gates have values close to 1 and therefore difficult to carry information to later time. As the initial frames of an utterance usually contain helpful information such as background noise, this might cause DecGRC to be degraded compared to the global attentions. The last two plots in Fig. 2 show that the update gate values of DecGRC mostly changed near the attention region. As the update gates rapidly decreased after the attention region, tight attention endpoints could easily be found by setting the threshold value approximately in a range of [0.001, 0.2]. For instance, with an inference threshold \( \nu = 0.01 \) in Fig. 2, the total number of steps in the for loop in Alg. 1 was 459, which was approximately 54% of \( TU = 13 \times 65 = 845 \). It implies that insignificant time indices were properly ignored during the inference.

E. Ablation study on DecGRC inference threshold

We evaluated WERs of DecGRC models for different threshold values, and the results are summarized in Tbl. II. Setting the threshold to a value larger than 0.2 was found to be detrimental to the performance on the BiLSTM encoder (E8), with larger thresholds giving higher WERs. It means that some encoded vectors in the correct attention region were ignored due to the high threshold, as shown in the last two plots of Fig. 2. Impressively, the best performance was obtained with \( \nu \) between 0.001 and 0.1, not \( \nu = 0 \). This may be attributed to the fact that the thresholding not only reduced the latency, but also eliminated undesirable updates after the correct attention region. With thresholds higher than the best-performing threshold, the latency could be further reduced by taking the performance penalty, and vice versa.

The best-performing threshold on the LC-BiLSTM encoder (E18) was \( \nu = 0.08 \), which means that the optimal threshold for performance depends on the model architecture, thus threshold searching is required before test phase. Nevertheless, as the beam search inference on the dev set took less than 15 minutes using a single GPU, the time spent for the tuning process of the threshold was no more than 2.5 hours, which is much shorter than the model training time; a single epoch of training took 9 hours on average, and the total time for training a model from scratch was more than 5 days.

V. Conclusion

We proposed a novel softmax-free global attention method called GRC, and its variant for online attention, namely DecGRC. Unlike the conventional online attentions, DecGRC introduces no additional hyperparameter to be tuned at the training phase. Thus DecGRC does not require multiple trials of training, saving time for model preparation. Moreover at the inference of DecGRC, the tradeoff between ASR latency and performance can be controlled by adapting the scalar threshold which is related to the attention endpoint decision, whereas the conventional online attentions are not capable of changing the endpoint decision rule at test phase. Both GRC and DecGRC showed comparable ASR performance to the conventional global attentions.

For further research, the proposed attention methods will be investigated in various applications which leverage AED models. We are particularly interested in applying DecGRC to simultaneous machine translation [30] and real-time scene text recognition [31], where the latency can be reduced by exploiting an online attention method.

References

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