A stochastic model of epigenetic dynamics in somatic cell reprogramming

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Somatic cell reprogramming has dramatically changed stem cell research in recent years. The high pace of new findings in the field and an ever increasing amount of data from new high throughput techniques make it challenging to isolate core principles of the process. In order to analyze such mechanisms, we developed an abstract mechanistic model of a subset of the known regulatory processes during cell differentiation and production of induced pluripotent stem cells. This probabilistic Boolean network describes the interplay between gene expression, chromatin modifications, and DNA methylation. The model incorporates recent findings in epigenetics and partially reproduces experimentally observed reprogramming efficiencies and changes in methylation and chromatin remodeling. It enables us to investigate, how the temporal progression of the process is regulated. It also explicitly includes the transduction of factors using viral vectors and their silencing in reprogrammed cells, since this is still a standard procedure in somatic cell reprogramming. Based on the model we calculate an epigenetic landscape for probabilities of cell states. Simulation results show good reproduction of experimental observations during reprogramming, despite the simple structure of the model. An extensive analysis and introduced variations hint toward possible optimizations of the process that could push the technique closer to clinical applications. Faster changes in DNA methylation increase the speed of reprogramming at the expense of efficiency, while accelerated chromatin modifications moderately improve efficiency.

Keywords: differentiation and reprogramming, epigenetic landscape, induced pluripotent stem cells, mathematical modeling, probabilistic Boolean network

1. INTRODUCTION

Starting with the successful reprogramming of mouse and human fibroblasts to induced pluripotent stem cells (iPS; Takahashi, 2006; Takahashi et al., 2007), modifications of cell types have become extremely important in recent years. Manipulating the developmental state of cells transitioning from a differentiated to a pluripotent state or – as recently achieved (Vierbuchen et al., 2010) – to distinct differentiated cell types, opens the door for various clinical applications. Major roadblocks on the way to the clinic are the general inefficiency and slow pace of the process (Hanna et al., 2009).

While most of the reprogramming experiments today are still based on the viral transduction of the same four Yamanaka transcription factors SOX2, OCT4, KLF4, and cMYC (Takahashi, 2006), alternative techniques have been developed that improve the concept in various ways (Okita et al., 2008; Zhou et al., 2009).

Although direct reprogramming has made it possible to study the interplay of the networks regulating pluripotency in a defined environment, it is still not understood how the transition happens in detail. However, it has become clear that the reprogramming potential is not limited to specific cells in a culture, but rather that essentially every cell can be reprogrammed given enough time and the appropriate method (Hanna et al., 2009). A high proliferation rate seems to be beneficial to the process of overcoming the barriers in reprogramming (Hong et al., 2009; Kawamura et al., 2009; Marión et al., 2009). Moreover, efficiency could be improved by the addition of small molecules (Wang and Adjaye, 2010), some of which are also capable of replacing KLF4 and cMYC or even SOX2 (Ichida et al., 2009) in the process. Most of these discovered molecules act on the epigenetic modifications in the cells that fix them in their current developmental state. One of the most prominent drugs improving reprogramming is the histone deacetylase 1 (HDAC1) inhibitor valproic acid (VPA; Huangfu et al., 2008). The inhibition of HDAC1 seems to lower the epigenetic barrier between the cell states and facilitates the transition from one state to the other.

Pluripotency in general is regulated by an interplay of different mechanisms, the most important of which we will outline in detail in the following. First, transcriptional regulation, i.e., activation or inhibition of target gene activity by specific transcription factors, controls the expression of master regulators of pluripotency or differentiation. A second layer of control consists in DNA methylation of promoters of genes. Finally, the organization of chromatin in active or repressive structures represents the third mechanism.

The core transcriptional regulatory circuitry of pluripotency in human embryonic stem cells (hESCs) was first established by Boyer et al. (2005) and contained the master regulators of...
pluripotency OCT4, SOX2, and NANOG. These three transcription factors were found to interact in a mutually- and auto-activating fashion thereby promoting and maintaining pluripotency (Boyer et al., 2005; Loh et al., 2006). This regulatory circuitry has been extended in further studies to yield different larger networks regulating pluripotency (Ivanova et al., 2006; Zhou et al., 2007; Chavez et al., 2009).

DNA methylation of regulatory sequences, which silences gene promoters, is one of the known mechanisms in epigenetic regulation. This methylation is a major hindrance in reprogramming, because methylation marks cannot easily be removed, although there is evidence for active demethylation in reprogramming cells (Flöttmann et al., 2011) which we will further discuss below.

With the advent of next generation sequencing techniques there is a wealth of data accumulating on DNA methylations (“methylomes”) in different cell types (Lister et al., 2009, 2011; Laurent et al., 2010). These studies reported large differences between ES/iPS and differentiated cells in the methylation states of promoters of key pluripotency and developmental genes. Moreover, they identified a very slow reprogramming of methylation states with aberrant methylation persisting in reprogramming cells, which can thus be distinguished from fully reprogrammed or ES cells.

These remaining DNA methylation differences also limit the differentiation potential of the iPS cells and restrict their applications. A recent study also reported the occurrence of newly methylated aberrant sites that did neither occur in the source nor in the target (ES) cells (Nishino et al., 2011).

Comparable studies were not limited to DNA methylation. Histone modifications were also studied extensively, suggesting a close connection between DNA methylation and chromatin structure (Hawkins et al., 2010).

It has been found that there is a strong correlation between gene silencing histone modifications and DNA methylations in promoters of pluripotency regulators (Cedar and Bergman, 2009). However, the relationship between the two is still not fully understood. The connection is probably established by histone binding proteins such as G9a, which have histone methylation activity (HMT) and therefore facilitate the formation of heterochromatin. G9a can also recruit the de novo methyl transferases DNMT3A and DNMT3B to the nucleosome which in turn can methylate the gene promoters on the DNA. DNA methylation is thought to stabilize chromatin structure during mitosis through differential binding of proteins for closed or open chromatin (Cedar and Bergman, 2009) and it can also inhibit methylation of H3K4, an activating histone mark. Inheritance of histone modifications is coupled to the methylation pattern as it guides binding of certain HDACs (Fuks et al., 2000).

DNA methylation itself is sustained throughout DNA replication and methylation by virtue of DNMT1 and other associated proteins like NP95 by copying the methylation pattern of the template strand to the copied strand. Though this process is quite efficient, methylation can be lost in rapidly dividing cells and cells lacking DNMT1 (Monk et al., 1991).

The consequences of the complex interplay of the three mentioned regulatory mechanisms, i.e., transcriptional regulation, histone modifications leading to changes in chromatin structure, and DNA methylation, are not easy to understand. Mathematical modeling can help to unravel these complex interactions and explain how cell behavior is linked to the molecular mechanisms. Since we are dealing with an enormously complex system, we need to reduce it in order to discern the basic underlying features of the network. There have been various attempts to model certain parts of regulatory networks in great detail, which gave valuable insights into the dynamics of these subsystems (e.g., MacArthur and Please, 2008). However, since the whole process cannot be explained by breaking up the system into parts, we want to take a more holistic approach in this work and combine gene expression and epigenetic principles in one abstract model.

All the above mentioned regulatory processes only work correctly in an orchestrated manner. Regulatory structures in stem cells have been described by various models using different modeling approaches. There is a number of detailed models describing the interplay of regulatory genes in pluripotency and reprogramming, which help to understand the gene networks in detail and have elucidated the bistability of decisions taken in development and the influence of expression noise (Chickarmane et al., 2006; Chickarmane and Peterson, 2008; MacArthur et al., 2008; Kalmar et al., 2009). These models use ordinary differential equations to show the dynamics inside a small part of the whole machinery. There are also many studies describing regulation of differentiation into different lineages and the bifurcation dynamics preventing reprogramming (Roeder and Glauche, 2006; Huang et al., 2007; Duff et al., 2012). Moreover, there have been efforts to define the potential of cell states in theoretical models and use it to identify optimal routes of cell differentiation and reprogramming (Wang et al., 2010; Bhattacharya et al., 2011). Larger networks were just recently modeled using dynamic Bayesian networks and were used to predict improved reprogramming factor combinations (Chang et al., 2011).

A second class of more coarse grained models deals with transitions between cell states and how the system is shaped by self-organizing systems in the cells (Qu and Ortolena, 2008; Halley et al., 2009). These models are very conceptual and refrain from describing single gene interactions. There have also been efforts to characterize the processes in chromatin remodeling in a theoretical model, which showed that there must be a positive feedback in the formation of heterochromatin structure to explain its observed behavior (Dodd et al., 2007).

Looking at the experimental evidence in the literature it seems that the progression of reprogramming is governed by stochastic processes that prohibit or permit activation of pluripotency genes. For that reason, there have also been attempts to model it with noisy ordinary differential equations (MacArthur et al., 2008) or even as a stochastic process of state transitions (Hanna et al., 2009). In a more general approach (Artyomov et al., 2010) the authors explicitly modeled the space of cellular states as a binary tree with nodes for each cell state and the pluripotent state as the root of the tree. This study was the first to include gene regulation and epigenetic changes in one model and it could, among other things, explain the low efficiency of reprogramming.

We are going in a different direction by building an abstract model of the combined networks that govern pluripotency and reprogramming using well established modeling frameworks in a novel way (Figure 1). Our model is based on a standard Boolean
Figure 1 | General model structure. Transcriptional regulators that account for the activation of a certain cell state are combined into a module. We have four modules in the complete model: Two different differentiation modules A and B, the Pluripotency Module P for the main pluripotency network, and the exogenous reprogramming genes E. Each module is governed by the activity of the other modules as well as its epigenetic states.
choose one of the networks to update the state. The probability of a specific state as a function of states to probabilistic Boolean Networks, we will refer to Flöttmann et al. Modeling epigenetics in reprogramming of the time of its appearance. Every node is updated at every time point by application of a set of update functions \( F = \{F_1, \ldots, F_n\} \) that integrate the input information of edges on one node. In other words, the function \( F_i \) assigns a new state value to the node \( v_i \) at time \( t + 1 \), i.e., \( v_i(t + 1) \). They depend on the state of \( k \) input nodes with \( k \in [0, \ldots, n] \) at time \( t \).

There have been different approaches to address uncertainty and stochasticity in the Boolean framework (Shmulevich, 2002; Garg et al., 2009; Twardziok et al., 2010). We will follow the probabilistic Boolean network (PBN) approach proposed by (Shmulevich, 2002), but apply it in a slightly different way. Originally, probabilistic Boolean networks were designed to represent the uncertainty in knowledge about regulatory functions. If there is experimental data showing that both transcription factors A and B activate gene C, but it is unclear whether they can act separately or only in combination, then there is not only one determined logical function that can describe their interaction. In probabilistic Boolean networks this uncertainty is taken into account by relaxing the constraint of fixed update rules \( F_i \) and by permitting instead one or more functions per node. Thus, function \( F_i \) is replaced by a set of functions \( F_i = \{f^j_i\} \) with \( j \in \{1, \ldots, l(i)\} \), where \( f^j_i \) is a Boolean logic function and \( l(i) \) the total number of functions for node \( v_i \). In each update step the functions are chosen randomly according to their probability which we assign.

Our model uses this feature of probabilistic Boolean networks to represent two kinds of stochasticity. The first is the aforementioned uncertainty about the correct function to apply. By employing different possible functions and varying their probability we can see which of them fits the known data better. The second way how we use the probabilistic functions is to model dynamic features of the system. The single processes that influence a variable are split into different functions and we assign each of them a probability. That way we can adjust the probability of the activation of a variable under certain conditions instead of assigning it one fixed value. We can also easily split activation and inactivation into different functions. Depending on the influencing variables the probabilities of the state of the variable change.

### 2.2 SIMULATION

The implemented model is based on the probabilistic Boolean networks approach (Shmulevich, 2002). The complete model consists of \( n \) different variables, which are updated by Boolean rules in each time step. The rules all consist of AND, OR, and NOT connections between the different variables. In each time step one of the functions is chosen with its assigned probability to determine the next state of the variable. Probabilistic Boolean models can be simulated in different ways. Either one can simulate single trajectories of the model and analyze the results like the outcome of a stochastic experiment, or one can analyze the resulting Markov chain. All simulations were carried out using the R-Package BoolNet (Müssel et al., 2010).

The PBN can be viewed as an ensemble of \( N \) standard Boolean networks, where \( N = \prod_{i=1}^{l(i)} l(i) \). In each simulation step, we choose one of the networks to update the state. The probability of each network being chosen is the product of the probabilities of the chosen functions. The vector \( D^t = (D_1^t, \ldots, D_n^t) \) now comprises the probabilities of all \( r = 2^n \) states at time \( t \), i.e., the probability of the network to be in this state. We can define a \( (2^n \times 2^n) \) matrix \( A \), that contains the probability to transition from state \( i \) to state \( j \) given all possible networks. If there is no network allowing the transition \( i \rightarrow j \), \( A_{ij} = 0 \) otherwise \( A_{ij} \) is the sum of the probabilities of all the networks allowing this transition. Matrix \( A \) is a state transition matrix of a homogeneous Markov process. Thus, given a \( (1 \times 2^n) \) vector \( D^0 \) with a start probability for each state we can recursively simulate the system from \( t \) to \( t + 1 \) as equation \( (1) \) or as well directly deduce the value at \( t + 1 \) of this geometric progression \( (2) \):

\[
D^{t+1} = D^t \cdot A \\
D^{t+1} = D^0 \cdot A^{t+1}
\]

This kind of simulation enables us to follow transitions from a single state to all its successors, but also makes it possible to start in a distribution of states. The distribution approach is much closer to biological reality than one sharp state since we are simulating on a cell population level. We used the Markov simulations to find the stationary states or attractors of the system and to find states with transient high probabilities.

To visualize the probability distributions in our model we plotted the probability for each state at each time point \( t \) in a three-dimensional plot. To sort the states in a meaningful ordering, we defined a distance measure for states as explained below. This measure ensures that states that are biologically different, are further apart in the plot and those that differ only slightly are closer together. The outcome is similar to the so-called epigenetic landscape of the cell (Figure 2). In the next two sections we will describe the generation of the start state distributions and the aforementioned sorting of the states for plotting.

### 2.3 START STATES AND START DISTRIBUTIONS

Our main model contains 14 variables thus we are looking at a total of 16,384 \( (2^{14}) \) possible states. An appropriate start state for the simulation must take into account that a cell population is very unlikely to consist of one specific Boolean state only, even if we are looking at a pure population of one cell lineage. There is always noise in biological systems: Genes that are not necessarily needed can be transcriptionally inactivated in one cell, but can randomly be expressed in the other, by chance packed into heterochromatin structures or their promoter even be methylated while the state is still viable. Nonetheless, there seems to be an optimal configuration of gene expression patterns and epigenetic structures for every cell type in which the majority of the cells lie. To account for the biological noise, we attribute probabilities in the vector \( D^0 \) to states depending on their similarity to the optimal state yielding a normal distribution around the latter. In the next section we will define the similarity term and how we implemented it for our problem set.

### 2.4 SORTING THE STATES BY A SPECIFIC SIMILARITY MATCHING

A time course simulation of every state in the state space can be represented as a three-dimensional landscape where the states lie on the \( x \)-axis, the simulation time on the \( y \)-axis, and the probabilities...
**FIGURE 2 | The epigenetic landscape.** The x-axis shows all possible states of the model, sorted by similarity $\Sigma_i^{123}$ (Section 2.4) to the distinguished states, i.e., differentiated state A, differentiated state B, or pluripotent state P. The y-axis corresponds to simulation time steps, and the z-axis to state probabilities. (A) Reprogramming starting from one clearly defined state where A is active and the reprogramming factors are present. (B) Differentiation by the activation of module A through a weak signal.
Table 1 | Variables and states of our model.

|                  | m^e | m^f | m^h | m^p | m^a | m^he | m^hhe | m^m | m^p | m^a | m^he | m^hhe | m^pe | m^fpe | m^ne | m^he | m^hhe | dnmt | demeth |
|------------------|-----|-----|-----|-----|-----|-------|--------|-----|-----|-----|-------|--------|------|-------|------|-----|--------|------|--------|
| Pluripotent state S_1 | 0   | 1   | 1   | 1   | 0   | 0     | 1      | 1   | 1   | 0   | 1     | 1      | 0    | 1     | 1    | 1    | 1      |    |       |
| Differentiated state S_1 | 0   | 1   | 1   | 0   | 1   | 1     | 1      | 0   | 0   | 0   | 1     | 0      | 0    | 1     | 1    | 0    | 0      |    |       |
| Differentiated state S_2 | 0   | 1   | 1   | 0   | 1   | 1     | 1      | 0   | 1   | 1   | 0     | 0      | 0    | 1     | 0    | 0    | 0      | 0  | 1.0    |
| Weight vector W_1 | 0.5 | 0.5 | 0.5 | 2.0 | 10.0 | 5.0    | 2.0    | 2.0 | 2.0 | 2.0 | 0.5    | 5.0    | 2.0  | 2.0   | 2.0  | 0.5  | 5.0    | 1.0 | 1.0    |
| Weight vector W_1 | 0.5 | 0.5 | 0.5 | 2.0 | 2.0  | 2.0    | 2.0    | 2.0 | 2.0 | 2.0 | 2.0    | 2.0    | 2.0  | 2.0   | 2.0  | 2.0  | 2.0    | 1.0 | 1.0    |

The columns represent the model’s variables. In the rows, the pluripotent and the two differentiated states as Boolean states as well as the weight vectors explained in Section 2.4 and used for the state sorting in Figure 2 are shown.
FIGURE 3 | State space of the combined model of reprogramming. Time evolution of the model starting with an active differentiation network and active reprogramming genes. The figure only shows the states that are reached with a probability of $p \geq 10^{-4}$. The model has 2073 possible state transitions between these 149 states. Different phases can clearly be separated in the reprogramming process. In the beginning (yellow area) the epigenetic factors of the different modules are modified, but there is no change in gene expression yet. The second phase (dark yellow) represents the down-regulation of the differentiation module followed by the activation of the pluripotency module (blue area). The last step consists of the silencing of exogenous factors, that produces stable iPS cells (red area). There are some states that can lead to non-viable cells, in which no regulators are expressed at all (gray area). The bold blue arrows represent the shortest path to the main pluripotent state.

The modules contain many activating interactions between their members. A good example is the network of OCT4, SOX2, and NANOG that is responsible for sustaining pluripotency. These transcription factors bind a large number of shared targets as well as their own promoters. This leads to their mutual and autoactivation (Boyer et al., 2005). Similar interactions have been reported for master regulators of differentiated cell lines like PU-1 for erythrocytes (Nishimura et al., 2000; Okuno et al., 2005) or PPARγ for adipose tissue (Wu et al., 1999).

Interactions between these modules are often mutually repressive, as it was reported for GATA-1 and PU-1 (Rekhtman et al., 1999). The pluripotency module also represses differentiation factors. This mutual antagonism paired with auto-activation of the single modules is the basic structure of the transcription factor regulations in our model.

The basic findings underlying the logical rules in our model are summarized in Table 2. The epigenetic regulations that influence the expression level in general and specifically for each module are described in detail in the following.

Although there has been immense progress in the field of epigenetics in recent years, many of the regulatory mechanisms and their interactions are still enigmatic to researchers (Cedar and Bergman, 2009; Djuric and Ellis, 2010). In our model we explore different motifs of the epigenetic marks governing gene expression in development and reprogramming. The general mechanism implemented in the model follows the approach suggested by (Cedar and Bergman, 2009). Epigenetic dynamics emanate from the more rapidly changing states of the proteome of the cell. The expressed regulatory proteins and RNAs not only govern future expression profiles by direct action on promoters, but also change the more persistent epigenetic marks which then in turn redefine a new set of transcribed genes and, thus, of cellular proteins. In our model, the expression of genes that belong to the same module increases the chances of removing silencing marks on chromatin. Once the chromatin is in an open conformation, we assume there is a possibility to remove DNA methylation if it is also suppressing gene expression in the module. The process of silencing can happen if the genes of a module are not expressed. The module is then prone to methylation and formation of heterochromatin. If one of the silencing marks is set, it increases the chances of keeping it and setting the second mark as well. As described above, histone modifications and DNA methylations are strongly interconnected...
| Represented property                                      | Update rule                                                                 | Probability | Explanation                                                                                                                                 |
|----------------------------------------------------------|------------------------------------------------------------------------------|-------------|---------------------------------------------------------------------------------------------------------------------------------------------|
| Auto-activation of gene modules                           | $m_i^A(t+1) = m_i^A(t) \land \neg(m_i^B(t) \lor m_i^C(t)) \land \neg m_{ihc}(t)$ | 0.5/0.5     | Regulatory proteins are closely coregulated and are often connected by positive feedback loops. (Boyer et al., 2005; Chickarmane and Peterson, 2008; MacArthur et al., 2008) |
| Pluripotency module activating DNA methylation           | $dnhmt(t+1) = m_i^C(t) \lor m_i^B(t) \lor dnhmt(t)$                          | 0.99        | DNMT3 co-regulated with pluripotency genes. DNMT3 methylates unspecifically (Adewumi et al., 2007; Mah et al., 2011)                      |
| Mutual inhibition of gene modules                         | $m_i^A(t+1) = m_i^A(t) \land \neg(m_i^B(t) \lor m_i^C(t)) \land \neg m_{ihc}(t)$ | 0.5/0.5     | Master Regulators inhibit other master regulators, competing lineages repress each other (Nikwa et al., 2005; Raiston and Rossant, 2006; MacArthur et al., 2008) |
| Heterochromatin increases probability for DNA methylation| $m_{ihc}(t+1) = m_{ihc}(t) \lor dnhmt(t) \land m_{ihc}(t)$                  | 0.05        | Interaction via G9a complex: DNMT3A/B bind to nucleosomes with methylated histones such as H3K9me and methylates DNA (Cedar and Bergman, 2009) |
| Heterochromatin formation is inhibited by appropriate gene module | $m_{ihc}(t+1) = m_{ihc}(t) \land \neg m_{ihc}(t)$                          | 0.11        | G9a binds specific sequences (Epsztejn-Litman et al., 2008)                                                                                |
| DNA methylation increases probability for heterochromatin formation | $m_{ihc}(t+1) = m_{ihc}(t) \land m_{ihc}(t) \land m_{ihc}(t)$ | 0.17        | Promotes chromatin inheritance after mitosis (Thomson et al., 2010)                                                                       |
| DNA demethylation slower than other factors               | $m_{ihc}(t+1) = m_{ihc}(t) \land \text{demeth}(t)$                          | 0.02        | Passive cell cycle dependent demethylation through variable DNMT1 activity after mitosis (Li et al., 1992)                                |
| DNA demethylation is faster in euchromatin               | $m_{ihc}(t+1) = m_{ihc}(t) \land (\text{demeth}(t) \lor m_{ihc}(t))$        | 0.03        | Histone deacetylase (HDAC) inhibitor TSA induces global and specific DNA demethylation (Ou et al., 2007)                                  |
| Methylation not necessary to downregulate retroviral gene expression | $m_{ihc}(t+1) = -m_{ihc}(t) \lor m_{ihc}(t)$                               | 0.5         | Retroviral silencing is DNMT3A/B independent in the first 10 days of reprogramming (Pannell et al., 2000)                                 |
| Retroviral gene demethylation is very slow in absence of DNMT3A/B or DNMT1 | $m_{ihc}(t+1) = m_{ihc}(t) \land (\text{demeth}(t) \land \text{dnmt}(t))$ | 0.001       | A complex between HDAC and NANOG (NODE complex responsible for the silencing of developmental genes) could account for retroviral silencing (Hotta and Ellis, 2008; Liang et al., 2008) |
| Retroviral gene heterochromatin dynamics                 | $m_{ihc}(t+1) = m_{ihc}(t) \land m_{ihc}(t)$                               | 0.1         |                                                                                                                                              |

In bold, we represent the part of the variable’s update rule that reflects the modeled property referenced in the column Explanation. The column P contains the probabilities of the update rule.
This collaborative aspect of silencing creates a positive feedback loop, which promotes bimodality of the epigenetic states, meaning that there is a low probability to stay in a state where only one of the marks is set when the gene state is constant.

We assume that the DNA methylation of the promoter regions of the genes in one module are coregulated to a large degree, and are thus also characterized by one entity only. This variable follows rules which we derived from literature (Table 2; Figure 4). Activation of this variable means that the promoters are methylated which will inhibit gene expression. The activation of the DNA methylation status is governed by the presence of de novo methyl transferases DNMT3A/B which are summarized in the variable dnmt. However, dnmt is not the only variable influencing the DNA methylation state of a module. As described above, there are also other chromatin binding proteins influencing the likeliness of DNA methylation. We assume that all of these proteins combined are responsible for the current local chromatin structure and set the chromatin structure of the module as a modulating factor of the DNA methylation. This defines the activating update function, that – if chosen – can only activate the variable. If the DNA is already methylated, it can be demethylated by different mechanisms. For example, inefficiency of DNMT1 copying of methylation patterns is considered as passive demethylation (Monk et al., 1991). This process can only happen when cells are dividing, as it depends on DNA replication. However, there might also be active demethylation processes influencing the DNA methylation state as discovered recently (Table 2). In our model, we summarize these processes leading to demethylation of DNA in the variable demeth. All of the mentioned processes happen very slowly compared to transcription factor mediated changes in the regulation of expression, which is why we also introduced a function that does not alter the variable when it is chosen. This function gets a high probability compared to the rest. A combination of the above yields the following update functions for methylation of pluripotency genes:

\[
\begin{align*}
    m^A_m(t+1) &= m^A_m(t) \lor \text{dnmt}(t) \land m^A_m \\
    m^A_m(t+1) &= m^A_m(t) \land \text{demeth}(t) \lor m^A_m \\
    m^A_m(t+1) &= m^A_m(t) \land m^A_m \\
    m^F_m(t+1) &= m^F_m(t)
\end{align*}
\]

where $m^A_m$ and $m^F_m$ are the methylation and chromatin states of module $A$, respectively. Similar rules hold for modules $B$ and $P$ (modules as shown in Figure 1). Note that probabilities of the formulas sum up to 1.

The dnmt and demeth variables are governed by the following rules:

\[
\begin{align*}
    \text{dnmt}(t+1) &= m^F_e(t) \land m^F_e(t) \\
    \text{dnmt}(t+1) &= m^F_e(t) \lor \text{dnmt}(t)
\end{align*}
\]

Activation of pluripotency genes also leads to a higher cell division rate, a suppression of methylation maintenance and probably active demethylation, which also increases the chances of euchromatin formation. Without external influences (e.g., retroviral genes or signaling molecules), the structure of our model consists of three gene modules (P, A, B) inhibiting each other and each governed by their specific epigenetic states. The pluripotency (P) module regulates the activation of methylation and demethylation.
We consider neither single modifications on different sites nor different numbers of methyl groups on the residues. Chromatin changes are dependent on the expression of the module’s genes. If these genes are expressed, it is impossible to remodel the chromatin to a closed form. If they are not present, there is a chance of negative histone modification which is increased by present DNA methylation marks. In Boolean formulas these processes are described as

\[ \text{demeth}(t+1) = m^P_E(t) \lor m^P_m(t) \]
\[ \text{demeth}(t+1) = m^E_E(t) \lor m^E_m(t) \lor \text{demeth}(t) \]

where \( m^P_E \) and \( m^P_m \) are the expression of the pluripotency and the exogenous modules, respectively. Switching off these factors is very slow, because we assume that the influences implemented here are not the only influence on these variables and that they are active in many cell states.

Histone modifications are strongly simplified in our model. We consider neither single modifications on different sites nor different numbers of methyl groups on the residues. Chromatin changes are dependent on the expression of the module’s genes. If these genes are expressed, it is impossible to remodel the chromatin to a closed form. If they are not present, there is a chance of negative histone modification which is increased by present DNA methylation marks. In Boolean formulas these processes are described as

\[ m^A_E(t+1) = m^A_E(t) \lor m^A_m(t) \land \neg m^A_m(t) \]
\[ m^A_m(t+1) = m^A_m(t) \lor \neg m^A_m(t) \]
\[ m^A_E(t+1) = m^A_E(t) \land \neg m^A_m(t) \]
\[ m^A_m(t+1) = m^A_m(t) \]

where \( m^A \) is the expression of module A, \( m^A_\text{hc} \) the chromatin state, and \( m^A_m \) is the DNA methylation of the module respectively. Following these rules the DNA methylation in a module increases the chance of forming and keeping heterochromatin, independent of the chosen parameters. The same is true for the chances of methylation, which are dependent on the chromatin state of the module as well. Thus, the epigenetic states are mutually dependent on each other, and are also reigned by the states of their expressed genes.

In turn, the expression of a module is governed by its epigenetic states. If the gene is located in heterochromatin and methylated it is marked inactive and cannot be activated by any composition of transcription factors. If both epigenetic sub-modules are inactive, the expression of the genes in the next time step only depends on the transcription factors. If the gene is in heterochromatin and not methylated or vice versa, there is still a chance that it is expressed, given the right transcription factors. We implemented these rules for all modules by the following Boolean formulas:

\[ m^A_E(t+1) = m^A_E(t) \land \neg (m^E_m(t) \lor m^P_m(t)) \land \neg m^A_m(t) \]
\[ m^A_m(t+1) = m^A_m(t) \land \neg (m^P_m(t) \lor m^E_m(t)) \land \neg m^A_m(t) \]

The activation of the pluripotency network by the transduced gene cocktail is also modeled explicitly. The pluripotency network has a small chance of being activated by the artificially introduced genes. These exogenic factors are deactivated when the cell has reached a pluripotent state with the pluripotency module turned on and all differentiated modules turned off. The probability of activation is rather small compared to the probability of the pluripotency module activating itself. Since only a small subset of pluripotency regulators is transduced in reprogramming experiments (usually 4 transcription factors) we assume that the activation is happening rarely. The probability is directly connected to the number of reprogramming factors transcribed, it can be increased to model the influence of additional NANOG transcription, which has been shown to be beneficial to the efficiency of reprogramming (Hanna et al., 2009).

The deactivation of the transduced genes is achieved by silencing of their promoters through methylation and chromatin remodeling by histone deacetylation (For a review, see Hotta and Ellis, 2008). In our model this process is triggered when the cell reaches the iPS expression profile.

Since the transduced genes differ from the endogenous pluripotency genes in their promoter region, some changes regarding their transcriptional repression and interactions of methylation and chromatin remodeling need to be done in comparison to the other modules.

Due to the viral promoters the expression of the retroviral genes only depends on their chromatin and methylation state and not on any transcriptional inhibitors or activators.

\[ m^E_E(t+1) = m^E_m(t) \lor m^P_m(t) \]
\[ m^E_m(t+1) = m^E_m(t) \land m^E_m(t) \]

The rules for methylation of the promoter of the exogenous genes are very similar to the ones of the other modules except for the probabilities which we chose to be smaller for \( dnmt \) and heterochromatin dependent DNA methylation. This is due to the finding that after reprogramming, the retroviral genes can still be active (class I iPSCs) or be silenced and thus fully reprogrammed (class II iPSCs; Niwa, 2007; Mikkelsen et al., 2008) which suggests that methylation of the viral promoters might not be fast and complete which would lead to quick silencing. Moreover, methylation does not seem to be needed to downregulate the activity of the retroviral genes according to Pannell et al. (2000) which accounts for these low probabilities as well.

Similar to the other modules, we also introduced slow, cell cycle dependent DNA demethylation induced by variable expression of \( DNMT1 \) after mitosis (Li et al., 1992; Table 2).

Since the remaining update rules for DNA methylation stay the same with the sole difference of lower probability in comparison to the other modules, this is the only structural difference:

\[ m^E_m(t+1) = m^E_m(t) \land (\neg \text{demeth}(t) \lor \text{dnmt}(t)) \]

The chromatin modification rules of the retroviral genes mainly depend on their own methylation state (just like the other modules) and on the expression of the endogenous pluripotency genes. We hypothesize this interaction to be mediated by a complex similar to the so-called NANOG and OCT4 associated deacetylase (NODE) complex or by this complex itself. It consists of a histone deacetylase (HDAC) and NANOG or OCT4 (Liang et al., 2008) and was found to catalyze histone deacetylation on developmental target genes thereby leading to heterochromatin formation. The hypothesis that this complex or at least one with very similar properties and behavior is responsible for retroviral gene silencing is based on the fact that \( de \) novo DNA methylation is not necessary for retroviral silencing as mentioned above (Pannell et al., 2000) and that there seems to be a complex of NANOG and the HDAC which is responsible for this process (Hotta and Ellis, 2008). Thus,
the only update rule differing from the other modules regarding
the heterochromatin structure depends on the expression of the
pluripotency module P:

\[ m_{\text{ch}}(t+1) = m_{\text{ch}}(t) \lor m_{\text{ch}}^P(t) \]  (12)

which completes our set of update rules.

3.2. SIMULATIONS OF A SINGLE MODULE

The basic building blocks of our model are modules of genes and
their epigenetic modifications. To analyze the general behavior
of these sub-networks, we start with simulations of the separate
blocks before describing different combinations of these.

A module consists of three nodes – the expression node, the
DNA methylation node, and the chromatin structure node – with
the DNA methylation node being connected to the main epige-
netic modifier variables namely \( \text{dnmt} \) and \( \text{demeth} \) (represented by
their actions, i.e., DNA methylation or DNA demethylation respect-
ively in Figure 1). We distinguish two different cases to describe
the complete set of different modules. First, there are the entities
A and B that only regulate their own expression and do not regulate
the expression of \( \text{dnmt} \) and \( \text{demeth} \), which are the components
responsible for differentiation. The second class of modules are
the pluripotency regulators \( P \), which regulate their own activation,
but also influence the activity of epigenetic modifiers.

Unsurprisingly, we found the differences in behavior between
the two classes to be substantial. We analyzed the modules under
different conditions, different parameter settings, and applied
disturbances like knockout or overexpression experiments and
quantified the effects in regard to the outcome distributions. For
each one of them, we built a model containing only the respective
module and external signals influencing it.

The pluripotency module \( P \) is the central point, as it has the
strongest connections to the main regulators of epigenetics \( \text{demeth} \)
and \( \text{dnmt} \). Its dynamic behavior and steady states reflect various
experimental results. The state in which the pluripotency module
is active is stable. Even if the chromatin state is set to heterochro-
matin, the model has a high chance to return to the pluripotent
state. This change in DNA methylation is activated, which silences
the genes and also locks the states of chromatin in the silencing
state. If one of the other genes is constantly expressed, the module
is suppressed by this gene and silenced by its epigenetic factors.
A relatively large fraction of cells is transferred to the respective
state. This shift happens rather fast, because during the activation
of the pluripotency genes the entities that enable changes in the
methylation states are active and are disabled in the resulting states
(Figure 5).

All modules are stable if their respective genes are the only ones
expressed and there are no further disturbances. The behavior of
the modules \( A \) and \( B \) in the unperturbed state is very similar to the
pluripotency module \( P \), but they are also more stable when per-
turbed. If one of the other non-pluripotency modules is switched
on – or over-expressed – the genes of the module are repressed,
but not irreversibly silenced. The gene is silenced quickly, and
the chromatin state changes to heterochromatin. But this state
cannot be stabilized by the formation of methylated DNA and is
therefore dynamically changing and after a few steps it reaches an
equilibrium (Figure 6B).

The response of the differentiation modules \( A \) and \( B \) is dif-
ferent for overexpression of pluripotency genes. If in a module
of differentiation the pluripotency genes are over-expressed – a
situation comparable to simplified reprogramming – the mod-
ule’s epigenetic factors enter a hyperdynamic state while its gene
expression is repressed (Figure 6A). This state has been observed in
differentiation genes in pluripotent cells (Niwa, 2007). The active
methylation factors enable changes in DNA methylation states and
in the equilibrium state there is a relatively high probability to be
in a methylated state for the module \( A \). If the signal is switched off
after some time the system will not return to the start state com-
pletely, but will be locked in non-physiological undesired states
where no genes are expressed anymore.

Overexpression of reprogramming factors has a strong effect
on other modules, that can already be witnessed in this small sub-
model. The question remains why the efficiency of reprogramming
is so low when it seems to work so quickly and effectively in single
modules. To tackle that question, we need to combine the single
modules \( A, B, \) and \( P \) to a model of the different competing net-
works in the cell and we also need to introduce the reprogramming
factors module \( E \) and its very own regulation to the system.

Changing key parameters of the system we will clarify which
alterations have the strongest effects on the systems behavior. For
example changing the probabilities of either changes in DNA
methylation or chromatin remodeling has very different effects
on the outcome of simulations.

3.3. STABLE CELL STATES AND DIFFERENTIATION OF COMBINED

MODULES

When combining the single modules to a more complex model
of two differentiated states and the pluripotency network \( A, B,
\) \( P \) model; Figure 1 without the exogenous factors, we see more
complex dynamics of state transitions. Gene expression in each
module is mutually exclusive with all other modules and a module
that is shut off once can only be activated by an external sig-
nal combined with epigenetic activation. The steady state of the
pluripotency module consists of a number of different states, that
represent the hyperdynamic characteristics in epigenetic factors of
the pluripotent cells (Mesner et al., 2006). These states have dif-
ferent probabilities to differentiate, depending on the current epi-
getic configuration. Similar kinds of population differences have
been shown for pluripotent cells and the expression of \textit{NANOG}
(Kalmar et al., 2009).

Since we already include three different levels of regulation in
our model, we refrain from adding detailed signaling pathways to
the system to regulate differentiation. We simulate differentiation
by simply activating the gene expression of gene module \( A \) with a
certain probability. This causes the system to leave the pluripotent
state very fast. After about 300 time steps it reaches its steady state
with the differentiated state being the main attractor (Figure 2A).
The system also reaches a state, in which all proteins are unex-
pressed. This state is reached because the differentiation signal is
strongly simplified and does not guarantee the correct timing of
events. If the pluripotency genes are switched off before the cor-
rect methylation pattern is in place, differentiation related genes
may not yet be properly expressed while pluripotency genes and
thus de novo DNA methylation and pluripotency related DNA
FIGURE 5 | Dynamics (A) and state space (B) of the pluripotency module during overexpression of differentiation factors. The network quickly leaves the pluripotent state and passes across a number of transient states into two different attractors. The node in blue (lower right) is a point attractor in the completely differentiated state and the nodes in brown are part of a cyclic attractor consisting of the unmethylated state in either a euchromatin or heterochromatin structure.

3.4. INTEGRATING REPROGRAMMING FACTORS

To analyze reprogramming, we combined the four single modules, i.e., the retroviral transcription factors E, the endogenous pluripotency genes P, and the two model cell lineages A and B into one model (Figure 1). We simulated the model in a Markov simulation for various starting distributions and systematically analyzed the temporal dynamics of the model for typical start scenarios.

First, we analyzed the situation in which the system is initialized with only one defined state that corresponds to either one of the two cell lineages A and B, i.e., the state, where the set of master regulator genes associated with lineage A is expressed, unmethylated, and in an open chromatin configuration, while the module for lineage B and for exogenous (E) and endogenous (P) pluripotency genes has the opposite configuration, meaning the genes are downregulated, methylated, and in a closed chromatin formation. For this specific start state, the network remains in its differentiated cell lineage over the complete time of simulation, i.e., the defined cell lineage is stable without any outer perturbation (data not shown).

Second, when the simulation starts from a state that corresponds to the fully reprogrammed cells, i.e., where module P has the active configuration, while the other modules are silenced, we observe a shift of states into states which are closely related (visualized by their proximity to the pluripotency state in the epigenetic landscape) to the pluripotency state. This behavior can be...
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FIGURE 6 | Dynamics and state space of single modules of differentiation regulators. (A) Time course of a differentiation module with the constant activation of the pluripotency genes included. Methylation and demethylation are activated, the module’s genes are silenced and the model reaches an equilibrium in a hyperdynamic state switching between open and closed chromatin and varying DNA methylation. (B) Overexpression of another differentiation module leads to silencing of the gene, but does not enable methylation changes.

observed in iPSCs and ESCs as well and is often referred to as a hyperdynamic plasticity. The cells have a fast changing chromatin structure in general and different methylation states on several loci (Meshorer et al., 2006). This plasticity leads to a distribution across different states in our model as there is no single point attractor. This effect may also be responsible for the priming of iPSCs to quickly differentiate into various different cell types upon external signals (Ang et al., 2011), as we also observe states that can more easily differentiate than the defined pluripotent state.

The third focus of our simulation was the model starting in the sharp states of the differentiated cell lineages when the retroviral transcription factors are expressed, unmethylated, and in open chromatin. These simulations can be related to classical direct reprogramming. As shown in Figure 2B, the starting state will be left quickly for transient states that lie along the path to pluripotent cells. When analyzing the landscape it becomes clear that cells will transit into states that resemble pluripotent cells more and more until they eventually reach the fully reprogrammed state with a certain probability. This probability can be considered as the reprogramming efficiency that increases with time (or cell cycles) as demonstrated before by Hanna et al. (2009). The state space of the simulation (Figure 3) reveals further details about the timing and order of the states that are passed on the way to reprogrammed cells. Since we are dealing with a model of 14 variables, the whole state space has 2\(^{14}\) states and since we use a probabilistic approach it could in theory be fully connected, i.e., every node of the state space could possibly have 2\(^{14}\) outgoing and incoming edges. Therefore we only show those states that can be reached from our starting state, and reach a probability larger than 0.0001 in the course of the simulation. These most relevant states are the ones that some cells will probably pass during the process of becoming iPSC cells. Surprisingly these states clearly show different events that are crucial in the reprogramming process and resemble the order of events described in the literature (Papp and Plath, 2011). We simulated the model over 500 time steps, until it came close to a steady state of probabilities. The states that have the highest probability to be reached in the beginning (time steps \(\sim1 – 100\)) show a slow unpacking of the pluripotency genes, but about 10% also show modifications to the genes in the other lineage. After this stage all cells can enter the next phase which lasts for about 150 time steps. Nearly all states in this phase share the property that the differentiation genes are already shut down, but endogenous pluripotency genes are still silenced. From this stage there is a non-negligible possibility that the cells enter a non-functional state where nothing is expressed anymore, and which cannot be left. This state creates a small attractor that prevents the cells from successful reprogramming. The phase that follows with a much higher probability is the first stage of reprogrammed states. Cells in this state have been characterized as class I iPS cells (Niwa, 2007; Mikkelsen et al., 2008), as they express the endogenous pluripotency genes, but also still express the exogenous reprogramming cocktail that is not epigenetically silenced yet. From these states there is a slow transition to the states with a stable silencing of the exogenous
factors expression of pluripotency genes, and a hyperdynamic state in the differentiation modules. Cells reaching one of these states can have taken any existing path through the state space. In the visualized subspace, which makes up about half of the states reachable from the start state, there are 146 states and 2473 edges with only one connected component. As there are so many possibilities, the probability for each path is infinitesimally small. The most probable single path from the start state to the iPST state only has a probability of $9.3 \times 10^{-12}$ and consists of 7 state transitions. When looking at the state space structure it becomes obvious that the phases described above cluster together in the graph and that some states are much more central to the transition than others. Most states are not essential to the reprogramming, since there are nearly always paths that can avoid them. But there is one transition that is absolutely essential for reprogramming. This is the transient activation of the pluripotency module relatively early in the process after removal of their methylation marks. This enables the suppression of the differentiation genes and enables further reprogramming.

At the end of the process there is a large probability that cells are in the reprogrammed state. This corresponds to the findings by (Hanna et al., 2009), who showed that in a drug inducible reprogramming system all cells are able to reprogram given enough time.

As illustrated by the most probable path, not all of the described phases will be passed by all cells. There is often the probability of shortcuts like the one shown. In cells with a demethylation of all modules in an early phase, the pluripotency genes can be activated much faster compared to the rest.

As described in the materials and methods section, when looking at cell populations even of defined cell lineages, we are always dealing with a distribution of slightly different cells which can or cannot express certain factors and whose chromatin and methylation structure might be slightly different. Due to this fact, it might be more appropriate to characterize start distributions rather than sharp start states. We already described above how these distributions are generated. Interestingly, when starting in these distributions for differentiated cell lineages, in the absence of the retroviral genes we can observe a maintenance of a distribution around the differentiated state which accounts for stable cell lineages. When simulated from a distribution of states around the pluripotent state $P$ the system also reaches the hyperdynamic state distribution mentioned above. However, we have to make sure that the retroviral genes are silenced because their expression ultimately results in reprogramming (Figure 7).

### 3.5. Parameter Variations of the Model

In order to analyze the stability of our model and its behavior upon parameter variation, we varied the strength of the epigenetic modifications, i.e., DNA methylation and chromatin changes. We defined a parameter range including the parameters of our main model, a decreased and an increased probability of changes in methylation and heterochromatin formation and analyzed the effect on the reprogramming efficiency (Figure 8).

Interestingly, we can observe that in the time range of 2000 time steps our main model nearly seems to have a maximal saturation for its reprogramming efficiency which is only very slightly surpassed by increasing the probability for euchromatin formation. This increase could experimentally be reached through a heterochromatin formation inhibiting agent such as VPA (Section 1; Table 3).

However, the reprogramming timing can obviously be influenced by parameter variations. While an increase in methylation dynamics, i.e., faster demethylation, speeds up the reprogramming process with a reprogramming efficiency peaking at approximately 0.8 after 2000 time steps, we observe slower reprogramming for increased probabilities of heterochromatin formation and DNA methylation.

### 3.6. Structural Modifications of the Model

To check the sensitivity of the model to structural modifications and how its behavior corresponds to responses of reprogramming cells in reality, we searched the literature for various experiments that can be mimicked by slight modifications (Table 3).

In the following sections we describe such modifications and their effects on the reprogramming process with a focus on efficiency.

#### 3.6.1. Spontaneous Methylation

Since the exact mechanism of action of DNMTs in DNA methylation is still not fully understood, we modified the model to include spontaneous methylation. Hence, we introduced an interaction

![Figure 7](image-url)
that accounts for methylation of the different modules by \textit{dnmt} independently of other factors with a certain probability.

We found that in comparison to the original model, there was an overall decrease in the reprogramming efficiency, i.e., the steady state probability is approximately 10 times lower than in the original model after 500 time steps. However, the spontaneous methylation model reaches its steady state distribution slightly faster. Another interesting feature of the spontaneous methylation model is the fact, that it reaches a new specific state with a high probability. In this state, which we will call the undefined state, all modules are silenced except for the retroviral ones. We will discuss this state below.

3.6.2. Spontaneous heterochromatin formation

Similar to DNA methylation, the exact mechanisms of chromatin modifications are still a matter of debate. In our model, introducing spontaneous formation of heterochromatin as an independent term is a general de-regulation of these mechanisms, that could happen during reprogramming due to factor induction.

Even more pronounced than in the spontaneous methylation model, the steady state reprogramming efficiency is more than 40 times lower than in the original model. However, interestingly, in the first 50 time steps the probability to be in a reprogrammed state is higher than in the original or the methylation model and it is only at later time points that this changes. This may be due to the fact that the differentiation related state is downregulated much faster (results not shown). As in the methylation model, the undefined state mentioned above is also attained with a high probability.

3.6.3. Spontaneous demethylation

In contrast to DNA methylation and chromatin modifications, which have been in the focus of research for many years already, active DNA demethylation has long remained in the dark until recent discoveries have unraveled a new perspective. Thus, DNA demethylation seems possible via the intermediate 5-hydroxymethylcytosine and different enzyme driven modifications which transform it back to unmethylated cytosine (Bhutani et al., 2011). To account for uncertainty in spontaneous demethylation, we transformed the modules of the model in order to be able to randomly lose their methylation with a certain probability.

Of all our model variants, spontaneous demethylation reaches the highest reprogramming efficiency after 500 time steps although it is still 3–4 times lower than in the original model. Interestingly, this model variant shows a slightly different behavior than the two previous ones. Although its reprogramming efficiency stands back behind the original model in every time point, its differentiated state shows a fast decrease at the beginning, followed by a much longer second phase of slow decay very similar, in fact, to the reprogramming experiment of the original model (Figure 8).

3.6.4. Stronger interaction between methylation and heterochromatin

We analyzed the effects of the debated interaction between methylation and chromatin formation which we described above and in Table 2. The overall reprogramming efficiency after 500 time steps was approximately reduced by the factor 5. The dynamics of the differentiated state are very similar to the ones of the original model although it decreases even slower and remains with a higher probability at the end. Interestingly, another state is reached with a high probability, which is very similar to the differentiated state of the other cell lineage, except that the pluripotency module is already demethylated and in an open chromatin formation but still not expressed. This state is transiently present with a high probability which slightly decreases though over time. This phenomenon could be interpreted as trans-differentiation during reprogramming without passing the pluripotency state (Vierbuchen et al., 2010).

3.6.5. No methylation

In a model variant, where methylation has no influence on gene expression or heterochromatin formation we observe a very different behavior than in all the models before. In fact, without methylation effects, the model is neither able to reprogram anymore nor to differentiate. What we can observe instead is a re-distribution of the different start states, i.e., the pluripotency related or the differentiation related states, into very close similar states but no transition to any states that are further away in the state space. This is most likely due to the fact that methylation is needed in the long run to determine the heterochromatin structure after cell division and to fully silence gene expression. Without these features
Table 3 | Experimental findings from literature compared to simulation results.

| Experimental finding | Theoretical validation by our model |
|----------------------|------------------------------------|
| Somatic cells can be reprogrammed to iPSCs upon viral delivery of pluripotency factors with a very low efficiency (Takahashi, 2006) | Reprogramming experiment of our main model (Figure 2B) |
| iPSCs can be re-differentiated into various kinds of tissues (all three germ layers; Takahashi, 2006) | Differentiation experiment of our main model (Figure 2A) |
| ESCs have more euchromatin and accumulate high condensed heterochromatin as differentiation progresses (Francastel et al., 2000) | In the differentiation of the pluripotent state, which still consists of a distribution across several different chromatin and methylation configurations, we can observe a transition to more sharply defined states, which mostly include heterochromatin and methylation compositions (Figure 2A) |
| DNA methylation is essential for chromatin structure during development (Hashimshony et al., 2003) | In models lacking DNA methylation, differentiation as well as reprogramming are abolished and cells will not be able to pass to other states in the state space (Section 3.6.5) |
| Treatment of partially differentiated ES cells with the DNA demethylating agent 5-azacytidine (5-AzaC) induces de-differentiation (Tsujii-Takayama et al., 2004) | When starting from partly differentiated states in models with spontaneous demethylation mimicking 5-AzaC treatment, we observe de-differentiation and even efficient reprogramming (Section 3.6.3) |
| Knockdown of DnmtI reactivates retroviral genes (Mernig et al., 2007) | In models mimicking DnmtI knockdown (e.g., spontaneous demethylation in Section 3.6.3 or no methylation in Section 3.6.5 simulation from the iPS state leads to partial reactivation of retroviral genes) |
| Dnmt3a and Dnmt3b are not required for retroviral silencing in the first 10 days of reprogramming (Pannell et al., 2000; Hotta and Ellis, 2008) | In models without dnmt activity we can still observe silencing of retroviral genes (results not explicitly shown) |
| The histone deacetylase (HDAC) inhibitor valproic acid is capable of enhancing reprogramming efficiency (Huangfu et al., 2008) | In models where the probability for heterochromatin formation is downregulated (mimicking inhibition of HDAC) we observe a slight increase in the reprogramming efficiency (Figure 8) |

active modules cannot be silenced and thus inactive modules stay transcriptionally inhibited although they might be demethylated and in an open chromatin structure.

3.6.6. Polycomb repressor complexes (PRCs)

In an attempt to model the mechanisms of Polycomb repressor complexes (PRCs) described in Table 3 we introduced a positive interaction into the equation for heterochromatin formation depending on the pluripotency genes. In other words, the pluripotency genes directly promote heterochromatin formation of differentiation related genes, i.e., our lineage master regulators. Simulation and analysis of that particular model yielded a very similar result to the main model, which is probably due to the fact that the mutual transcriptional repression between our modules describes a very similar effect. Since this mechanism does not seem to significantly improve our model we decided to leave that interaction out.

3.6.7. Summary

The effects of the analyzed model variants on the reprogramming efficiency are summarized in Figure 8. For every model variant the reprogramming efficiency increases over time except for the model without methylation. What becomes apparent at first sight is that obviously all model variants seem to have a strongly decreased reprogramming efficiency after 2000 timesteps.

Overall, we find, that all variants resulted in de-regulating modifications of the original model, i.e., modifications that reduced the level of tight regulation of the epigenetic processes involved, which in turn have a direct effect on the expression of important genes. In the landscape of these model variants (which are not shown here), we could observe a general transition from a few defined states, that could be reached in the original model, to a strongly increased number of states. In the original model, we can reach a total of 2592 states after 500 time steps in a reprogramming simulation, while the spontaneous methylation model variant could reach 10,240 states in the same time. However, the efficiency of reprogramming was approximately 10 times lower (Figure 8) in the spontaneous methylation model. The 366 reached pluripotency related states in both models are the same except for their probability to be reached after 500 timesteps.

DISCUSSION

In this study we developed, to our knowledge, the first model of processes in somatic cell reprogramming that explicitly includes the virally transduced factors and their regulatory interactions. The model is also unique in its representation of the different epigenetic factors that regulate cell states and their interactions. Our modeling approach qualitatively reproduces experimental results from reprogramming as well as differentiation experiments. The probabilistic Boolean state space in combination with the epigenetic landscape plots of the simulations gives insights into different possible ways which reprogramming cells take in this scenario. Combined these visualizations can be related to the potential landscapes that have been developed for continuous modeling approaches. They show the direction the system is moving toward as well as the probability for each state to be reached under specific conditions. The stategraph also makes it possible to identify different phases during reprogramming that are important milestones.
These simulation phases are coherent with the sequence of events reported in many experiments. The reprogramming efficiency of the system seems high (p = 0.8 after 2000 time steps) compared to experimental results from transduction experiments, but one has to keep in mind that the model leaves out major experimental hurdles and regulatory mechanisms. We neither include immune response of cells nor varying transduction rates. The general efficiency shows a similar behavior to experiments done in inducible stem cell systems, which also showed sigmoidal efficiency curves with saturation at high levels. After a long simulation time we reach a high steady state of reprogrammed cells in a relatively broad distribution of states. Nevertheless, this high reprogramming rate indicates that there are mechanisms not included in our model that are suppressing reprogramming in differentiated cell

Differentiation in our model is also possible and happens a lot faster than reprogramming, although it is impaired by the lack of regulatory factors. In order to improve the representation of the course of differentiating cells the model would need to be extended by signaling pathways. This would enable a more precise modulation of the activity of the important model components and would moreover enable the system to sense the influence of external factors. Another interesting extension of the model would consist in the integration of further branches of differentiation for other cell lineages to depict the path from stem cells over progenitors to fully differentiated cells. These extensions are simplified by the modular structure of our model.

The model is very much centered on the mutual inhibition of master transcription factors and their connection to epigenetic factors, which is an important mechanism, but other regulatory processes, not captured by this approach, certainly play crucial roles during phenotype transitions. Cell types are generally viewed as different steady states of gene regulatory networks. This is reflected in the model by various attractors that represent different cell types. Nevertheless it does not account for cell types that express a mixture of regulatory genes, as for example progenitor cells would. These states can occur as cyclic attractors, but are unstable to stochastic perturbations and are therefore left quickly.

Because the model is very abstract, predictions cannot aim to completely reflect biological reality, but they can show trends and general effects that hold true for the modeled entities. The modifications we introduced show how the system reacts to perturbations in the epigenetic regulations. Most of the structural changes showed a devastating effect on the reprogramming efficiency, demonstrating the need of tight regulation of the process. The only two modifications, in which efficiency can be sustained at an adequate level, are those that increase the influence of the gene regulatory networks on the epigenetic factors.

Improvements of the reprogramming efficiency can only be achieved by two modifications. First, higher probabilities for changes in DNA methylation status lead to a faster increase of the reprogrammed cells, but also to a lower probability in the steady state. Therefore a de-regulation can have beneficial effects on the process, but also has drawbacks. Higher probabilities for changes in chromatin state lead to a mild increase in efficiency, resembling the effects of small molecules like VPA.

A better understanding of the underlying processes of somatic cell reprogramming is the key to a clinical application of iPS cells in the future. The proposed model, although very abstract and limited, goes a step into this direction. It outlines the possible epigenetic regulations that play a role in reprogramming, elucidates their connections, and partly explains experimental observations in reprogramming although it ignores large parts of the complex gene regulatory network of developmental genes.

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