The GOGREEN survey: Transition Galaxies and The Evolution of Environmental Quenching

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ABSTRACT

We measure the rate of environmentally-driven star formation quenching in galaxies at $z \sim 1$, using eleven massive ($M \approx 2 \times 10^{14} M_\odot$) galaxy clusters spanning a redshift range $1.0 < z < 1.4$ from the GOGREEN sample. We identify three different types of transition galaxies: "green valley" (GV) galaxies identified from their rest-frame $(NUV - V)$ and $(V - J)$ colours; "blue quiescent" (BQ) galaxies, found at the blue end of the quiescent sequence in $(U - V)$ and $(V - J)$ colour; and spectroscopic post-starburst (PSB) galaxies. We measure the abundance of these galaxies as a function of stellar mass and environment. For high stellar mass galaxies ($log M/M_\odot > 10.5$) we do not find any significant excess of transition galaxies in clusters, relative to a comparison field sample at the same redshift. It is likely that such galaxies were quenched prior to their accretion in the cluster, in group, filament or protocluster environments. For lower stellar mass galaxies ($9.5 < log M/M_\odot < 10.5$) there is a small but significant excess of transition galaxies in clusters, accounting for an additional $\sim 5 - 10$ per cent of the population compared with the field. We show that our data are consistent with a scenario in which 20–30 per cent of low-mass, star-forming galaxies in clusters are environmentally quenched every Gyr, and that this rate slowly declines from $z = 1$ to $z = 0$. While environmental quenching of these galaxies may include a long delay time during which star formation declines slowly, in most cases this must end with a rapid ($\tau < 1$ Gyr) decline in star formation rate.

Key words: galaxies: evolution, galaxies: star formation, galaxies: clusters:

1 INTRODUCTION

In an ΛCDM universe, structure evolution is driven by gravitational growth of dark matter haloes. Most of the elements necessary for galaxy formation under these circumstances have been understood for some time (White & Frenk 1991). In particular, the growth of galaxies is dominated by star formation, mergers and feedback, which largely decouple them from the growth of dark matter structures (e.g. Behroozi et al. 2013). We can directly observe this galactic growth through the evolution of the stellar mass function (SMF), which shows that much of the stellar mass in the local universe was already assembled by $z \sim 2$ (e.g. Fontana et al. 2006; Arnouts et al. 2007; Drory et al. 2009; Santini et al. 2012; Muzzin et al. 2013).

The star-formation rate (SFR) of star-forming galaxies is nearly proportional to stellar mass, at all redshifts to at least $z = 2.5$ (Salim et al. 2007; Noeske et al. 2007; Patel et al. 2009; Whitaker et al. 2012), yet the SMF of these galaxies evolves only modestly with time (e.g. Muzzin et al. 2013; McLeod et al. 2021). In contrast, the abundance of non-star-forming (passive, or quiescent) galaxies builds up rapidly with time. This indicates that there is a transition — quenching — of the galaxies from the blue cloud to the red sequence in colour–magnitude space as they stop forming stars (e.g. Bell et al. 2004; Brown et al. 2007; Faber et al. 2007). The bimodality in the SFR and colour distributions of galaxies implies that this transition must be fairly rapid (e.g. Wetzel et al. 2012). This transition rate is strongly dependent on stellar mass, and galaxies with high masses are more likely to be quenched (e.g. Takamiya et al. 1995; Strateva et al. 2001; Muzzin et al. 2013). However, the fraction of quiescent galaxies also depends on their environment (e.g. Lewis et al. 2002; Gómez et al. 2003; Baldry et al. 2006) such that, at fixed stellar mass, galaxies in dense environments are more likely to be quiescent. This suggests that additional environmental quenching processes are contributing to the...
build up of the red sequence in clusters. Empirically, the additional environmental quenching at \( z = 0 \) is separable from the stellar mass dependence (Baldry et al. 2006; Peng et al. 2010), though this may not be true at \( z \gtrsim 0.7 \) (e.g. Balogh et al. 2016; Kawinwanichakij et al. 2017).

The intermediate region between the star-forming and quiescent phases of galaxy growth can provide constraints on the nature of galaxy transformations and the rate at which galaxies undergo them. Such transition galaxies have often been used to trace the quenching rate over time and as a function of stellar mass (Tran et al. 2004; Pattarakijwanich et al. 2016; Wild et al. 2016, 2020; Socolovsky et al. 2018). The slow, undisturbed fading of star formation in galaxies may account for most of the quiescent population (e.g. Gladders et al. 2013), though there is also evidence that some galaxies undergo a more rapid transformation (e.g. Belli et al. 2019). The redshift evolution of these quenching pathways remains relatively unconstrained. This is in part due to differing definitions used to select transitioning galaxies, and to different assumptions about their parent populations (e.g. Belli et al. 2019; Carnall et al. 2019).

Our focus here lies in the environmental component of galaxy evolution. There is a large body of literature on the use of transition galaxies to trace quenching in dense environments (e.g. Zabludoff et al. 1996; Balogh et al. 1999; Poggianti et al. 1999, 2009; Hogg et al. 2006; Yan et al. 2009a; Mok et al. 2013, 2014; Paccagnella et al. 2017; Paccagnella et al. 2019). This work was pioneered with the discovery of "E+A" galaxies in clusters (Dressler & Gunn 1983, 1992; Couch & Sharples 1987); these are galaxies that have strong Balmer absorption lines in their spectra, indicative of recent star formation, but no signs of ongoing star formation since they lack [OII] or H\(_\alpha\) emission. Those E+A galaxies with the strongest Balmer absorption lines require a burst of star formation to precede a rapid quenching event (Couch & Sharples 1987; Yang et al. 2008; French et al. 2018), which has led to their classification as "post-starburst".

The identification of traditional E+A galaxies requires spectroscopy. An alternative approach has been to use the "green valley" in photometric data. Originally the green valley was defined as the region between the red sequence and blue cloud in a colour-colour space at \( 1 < z < 1.5 \). This approach is taken to capture all galaxies as they pass from star-forming to quiescence, independent of the quenching mechanism. It therefore provides a complete census of the transition rate, though it is not "pure" in the sense that it will also include substantial "contamination" from edge-on spiral galaxies and galaxies with slowly declining SFRs (e.g. Schawinski et al. 2014). We therefore complement this with analysis of both "blue quiescent" (BQ) galaxies (Belli et al. 2019; Carnall et al. 2019) and spectroscopic post-starburst galaxies (e.g. Poggianti et al. 2006; Muzzin et al. 2014), to obtain a more complete picture of the recent quenching rate in these systems.

The structure of the paper is as follows. The data and galaxy selection are described in § 2. Our main results on the spatial distribution and SMF of green valley and other transition galaxies is presented in § 3. The implications of these results in the broader context of cluster galaxy evolution are discussed in § 4. Finally, we summarize our findings in § 5. Throughout this paper, we adopt the AB magnitude system, a Chabrier (2003) initial mass function (IMF), and a flat ΛCDM cosmology with \( H_0 = 70 \) km s\(^{-1}\) Mpc\(^{-1}\), \( \Omega_m = 0.3 \), and \( \Omega_\Lambda = 0.7 \), unless otherwise specified.

2 DATA

2.1 The GOGREEN Survey

The GOGREEN project is a spectroscopic and photometric survey of 21 galaxy clusters and groups at \( 1 < z < 1.5 \). For each system, deep (\( \gtrsim 24 \) AB) imaging is available in \( \sim 11 \) bands between \( u \) and 4.5\( \mu m \). The survey is built upon a large multi-object spectroscopic campaign with Gemini GMOS, targeting faint \( (z^\prime < 24.5 \text{ and } [3.6\mu m] < 22.5) \) galaxies over a 5.5′ field around each system. The spectroscopic sampling is unbiased with respect to galaxy type for \( M \geq 10^{10.2} \) M\(_{\odot} \), and secure redshifts are available for over 1500 galaxies. More details on the survey strategy and data are available in Balogh et al. (2017) and Balogh et al. (2021).

This work will focus on the eleven massive clusters\(^1\) in the GOGREEN sample at \( z < 1.4 \), selected from the SpARCS (Wilson et al. 2009; Muzzin et al. 2009; Demarco et al. 2010) and SPT (Brodwin et al. 2010; Foley et al. 2011; Stalder et al. 2013) surveys. With one exception (SpARCS1034, which has \( \sigma = 250 \pm 30 \text{ km/s} \) based on only nine spectroscopic members), these systems have velocity dispersions of \( 500 < \sigma < 1200 \) (Balogh et al. 2021). The relevant cluster-specific parameters are provided in Table 1. This includes the cluster radius \( R_{200} \), defined as the radius within which the

\(^1\) At the time of writing, K-band imaging observations were not complete for the final cluster, SpARCS1033+5753.
In order to determine the equivalent widths of H\(\alpha\) absorption and [O II] emission, again following the methodology of Balogh et al. (1999). For [O II], we identify the presence or absence of emission using the difference in the Bayesian Information Criterion, \(\Delta BIC\), which measures the extent to which model fits that include an emission line are preferred, as described in Old et al. (2020).

### 2.2.1 Cluster membership

For the photometric sample, candidate cluster members are selected using a photometric redshift (\(\pm 0.16\)) and radius (< 1 Mpc) cut around the cluster centre. The redshift cut is similar to what is used in van der Burg et al. (2020), chosen as a suitable balance between including most genuine cluster members without too much contamination. Nonetheless, since this redshift range is wide, driven by the uncertainties on those redshifts, a statistical background subtraction is required for the cluster population even after this selection. Following van der Burg et al. (2013), we use the large spectroscopic subsample to derive a correction factor to the photometric sample in each radius or mass bin \(i\), as:

\[
\text{corr}_i = \frac{N_{i, \text{secure cluster}} + N_{i, \text{false negative}}}{N_{i, \text{secure cluster}} + N_{i, \text{false positive}}},
\]

where \(N_{i, \text{secure cluster}}\) are photometrically-selected and spectroscopically confirmed cluster members (\(|\Delta z_{\text{spec}}| < 0.02\)), \(N_{i, \text{false negative}}\) are spectroscopically confirmed cluster members that lie outside the ±0.16 photometric redshift selection, and \(N_{i, \text{false positive}}\) are galaxies that lie within the photometric redshift range but are spectroscopically confirmed to be foreground or background galaxies. We calculate this correction factor for each galaxy subpopulation under consideration (described in the following subsections). Throughout the paper we include all cluster galaxies, including the brightest cluster galaxy (BCG, which is sometimes omitted) in the analysis.

The comparison photometric field sample is selected from all galaxies with photometric redshifts \(1 < z < 1.5\) and at \(r > 1.5\) Mpc from the centre of each cluster. We do not excise galaxies at the cluster redshift, or spectroscopically confirmed members from this sample. This may not be perfectly representative of a random field sample, and will include some galaxies associated with the cluster outskirts and surrounding structures. We elect not to use a larger, more representative field sample like UltraVISTA (Muzzin et al. 2013); this ensures our definition of different populations, particularly the green valley, can be directly and fairly compared with the cluster sample in a straightforward way. Our results are insensitive to the quantitative details of how our field is defined (in terms of the radial cut or redshift limits), and we show in § 3.2 that the stellar mass functions we measure for quiescent and star forming galaxies are in excellent agreement with those of van der Burg et al. (2020). Thus we do not expect our conclusions to be qualitatively sensitive to the definition of the reference field sample.

When considering the spectroscopic subsample, we select cluster members as defined in Biviano et al. (2021). The field sample consists of all non-members with spectroscopic redshifts \(1 < z < 1.5\). We do not apply any incompleteness corrections to this sample, so integrated quantities should be treated with caution. Our main analysis considers the fraction of different galaxy types in bins of stellar mass, and this should be insensitive to such corrections above our spectroscopic completeness limit of \(M = 10^{10.2} M_{\odot}\).
Table 2. For each of the subpopulations considered in this paper, we present their definitions and sample size. The final column provides the number of candidate cluster members. For the photometric sample this includes all galaxies within 1 Mpc of the cluster centre and a redshift $|\Delta z_{\text{spec}}| < 0.16$. For the spectroscopic PSB we report the number of dynamically identified cluster members.

| Population       | Selection Criteria                                      | Total sample | Cluster members |
|------------------|---------------------------------------------------------|--------------|-----------------|
| Star-forming (SF)| $(NUV - V) < 2(V - J) + 1.1$                           | 1302         | 463             |
| Quiescent (Q)    | $(NUV - V) > 2(V - J) + 1.6$                           | 702          | 504             |
| Green Valley (GV)| $2(V - J) + 1.1 < (NUV - V) < 2(V - J) + 1.6$          | 257          | 125             |
| Blue Quiescent (BQ)| $(V - J) + 0.45 \leq (U - V) \leq (V - J) + 1.35$| 164          | 106             |
| (PSB)            | $(D4000 < 1.45) \cap (A_{BIC} < -10)$                   | 54           | 34              |

Figure 1. The left panel shows our cluster samples in the $NUV - VJ$ colour-colour plane that we use to define our primary Quiescent (Q), Star-forming (SF) and green valley (GV) populations. The BQ galaxies (orange squares) are selected in $U - V$ $(V - J)$ colour space, as identified by the orange filled box shown on the right panel. The spectroscopic post-starbursts (purple crosses) are selected by their [OII] emission and D4000 break. Large symbols indicate galaxies above the spectroscopic mass limit of $M = 10^{10.2} M_\odot$. We show extinction vectors for $A_V = 1$, assuming a Calzetti et al. (2000, solid line) or Cardelli et al. (1989, dashed line) extinction law.

2.2.2 Star-forming, Quiescent and Green Valley galaxies

We define three independent galaxy populations based on their positions in rest-frame $(NUV - V)$ and $(V - J)$ colour-colour space (Schawinski et al. 2014; Smedhurst et al. 2015; Moutard et al. 2018), hereafter referred to as $NUV - VJ$, as shown in the left panel of Figure 1. As has been discussed extensively in the literature, the galaxy distribution in this space shows two main populations. The relatively tightly localized clump of galaxies with the largest $(NUV - V)$ colours are identified with quiescent (Q) galaxies, while the more extended sequence running from lower left to upper right are primarily star-forming (SF) galaxies. We define an intermediate region – the green valley (GV) – that is approximately parallel to the SF sequence, as shown in Figure 1. The GV is deliberately chosen to span the entirety of the colour-colour space, to ensure that any galaxy transitioning from star-forming to quiescence must pass through it, regardless of the evolutionary path it takes. The width is arbitrarily defined, but selected to be a balance between making it small enough to reduce contamination from the other populations, while still wide enough to include a large population of transitioning galaxies. The definitions of these three populations are summarized in Table 2. The SF sequence, and our GV boundaries, are closely parallel to the extinction vector expected for a Calzetti et al. (2000) dust law, which should mitigate contamination of the GV from dusty SF galaxies. The steeper slope associated with a Cardelli et al. (1989) dust law could lead to more significant contamination at the upper end of the main sequence (but see § 3.1, below). These dust vectors are both shown on Figure 1.

The use of the $(NUV - V)$ colour diagnostic, providing more than five magnitudes of dynamic range between the bluest and reddest galaxies, is made possible by the very deep $V$ (> 25.3) and $g$ (> 26) band imaging of GOGREEN clusters (van der Burg et al. 2020), so that most galaxies above our mass limit are directly detected at wavelengths close to the rest-frame $NUV$. In Figure 2 we show the fraction of each galaxy type that is detected at $> 3\sigma$ in either the $g$–band (northern clusters, with Subaru Suprimecam imaging) or $V$–band (southern clusters, from VLT-VIMOS). For $M > 10^{10.5} M_\odot$, most SF and GV galaxies have rest $NUV$ detections. Those SF galaxies that are undetected are typically red, $(NUV - V) > 3.5$, and lie at the upper end of the SF sequence, where dust extinction is high. Importantly, even at the lowest stellar masses we probe, about a third of the GV galaxies are directly detected. Non-detections could, in principle, be redder in $(NUV - V)$ than predicted, though this colour...
is still constrained by the fit to the redder filters in the spectral energy distribution (SED).

### 2.2.3 Blue Quiescent Galaxies

We next consider another population defined photometrically, as galaxies at the blue end of the quiescent population identified in \( \text{UVJ} \) colour-colour space. This has been advocated by, for example, Belli et al. (2019), who use deep rest-frame optical spectroscopy of 24 quiescent galaxies at \( 1.5 < z < 2.5 \) to demonstrate that galaxies in this part of colour-colour space are distinctly younger than most of the quiescent population (see also Figure E1 in Webb et al. 2020), with mass-weighted stellar ages of \( 300 - 800 \) Myr. Belli et al. (2019) argue that galaxies passing through this space are a result of relatively fast quenching: assuming that dust disappears immediately after star formation stops, such galaxies will be very blue for a short time, until the remaining massive stars die out.

While Belli et al. (2019) and others refer to these as "post-starburst" galaxies, we prefer a more model-independent term, and will call them "Blue Quiescent" (BQ) Galaxies. We choose to adopt the same BQ selection definition as Belli et al. (2019), including using the \( \text{UV} - \text{V} \) or \( \text{NUV} - \text{V} \) and \( \text{NUV} - \text{J} \) classifications in § 2.2.2. The boundaries of the BQ population are given in Table 2 and shown on the right panel of Figure 1.

### 2.2.4 Spectroscopic Post-starburst Galaxies

The last population we consider are "post-starburst" (PSB) galaxies, based on the D4000 and \([\text{O II}]\) spectral indices (Muzzin et al. 2014), and thus limited to the spectroscopic sample. As Balmer absorption is difficult to measure reliably in low signal-to-noise ratio spectra, we follow Muzzin et al. (2012) and use the 4000 Å break strength limit \( \text{D4000} \geq 1.45 \), rather than \( \text{H}\beta \) strength, to identify young stellar populations. We identify the absence of \([\text{O II}]\) emission using the difference in the Bayesian Information Criterion, \( \Delta \text{BIC} > 10 \), where model fits without an emission line are strongly preferred, as described in Old et al. (2020). This is different from Muzzin et al. (2012), who identify lack of emission by inspection of each spectrum. We have tested the effects of varying the \( \Delta \text{BIC} \) threshold, or by adopting a threshold in rest-frame equivalent width, \( W_0(\text{O II}) \leq 5 \) Å. Our results and conclusions are not sensitive to this choice. Our final PSB definition is summarized in Table 2. We show where these galaxies are found in \( \text{UVJ} \) and \( \text{NUV} - \text{V} - \text{J} \) colour space as the purple crosses on Figure 1, and in the plane of \( U - V \) and D4000 in Figure 3. In general many of the spectroscopic PSB galaxies are quite red in \( \text{NUV} - \text{V} \) or \( U - V \) colours, clustered at the upper (red) end of the SF population in the \( U - V \)-D4000 plane.

### 3 RESULTS

#### 3.1 Characteristics of the candidate transition populations

Figures 1 and 3 show where each of the candidate transition populations — GV (green diamonds), BQ (orange squares) and PSB (purple crosses) — lie in the different colour spaces used to define them. These figures show that while there is some overlap between them, they are largely independent samples. The GV contains about a third of the BQ galaxies (and \( 22 \pm 6 \) per cent of GV galaxies are classified as BQ), but only \( \sim 10 \) per cent of the spectroscopic PSBs. Those BQ and PSB galaxies that do lie in the GV are at the blue end of that region.

The GV galaxies, identified in \( \text{NUV} - \text{V} - \text{J} \) space, are still largely found between the SF and Q galaxies in the \( \text{UVJ} \) diagram (right panel of Figure 1). This is notable because here the Calzetti et al. (2000) and Cardelli et al. (1989) extinction vectors are nearly identical, and again parallel to the SF sequence. If some of the GV galaxies identified in \( \text{NUV} - \text{V} - \text{J} \) are due to dusty SF galaxies with a Cardelli et al. (1989) extinction law, they would lie at the upper end of the SF sequence in the \( \text{UVJ} \) diagram. We do in fact find a few galaxies here, making up less than 5 per cent of the GV population.
The PSB galaxies overlap substantially with the BQ population and the blue end of the GV in both colour-colour diagrams, but they also extend into the Q domain. Interestingly, Figure 3 shows that both the BQ and GV galaxies typically have large D4000 break strengths characteristic of old populations, and larger than the threshold used to define PSB galaxies, despite their blue \((U - V)\) colours.

We compare the average of the available spectra for cluster members of each galaxy type, in Figure 4. The spectra are normalized to the wavelength range \(4115 < \lambda / \AA < 4125\) and then median-combined. For each combined spectrum we measure the D4000 index, and the rest-frame equivalent widths of [OII] emission and H\(\delta\) absorption as defined in Balogh et al. (1999). The results are shown in Table 3, both for the cluster sample shown in Figure 4, and for the corresponding field populations. All selections show relatively strong Balmer absorption lines characteristic of young stellar populations, though the uncertainties are large. As reflected in Figure 3, the GV and BQ galaxies exhibit significantly stronger D4000 than the PSB galaxies. The average cluster GV spectrum shows weak [OII] emission, which could indicate residual star formation but could also result from a somewhat heterogeneous population that includes some normal star-forming galaxies. The [OII] emission is stronger and more significant in the field GV and BQ samples.

Figures 1, 3 and 4 do not clearly identify a strict evolutionary sequence between the GV, BQ and PSB galaxies. The colour evolution of a galaxy is sensitive not only to its star formation rate evolution during quenching, but to assumptions about the dust distribution and its evolution, and its prior star formation history (e.g. Belli et al. 2019; French et al. 2018). It may be that these populations partly reflect different quenching "pathways". While it would be informative to use stellar population modeling to better understand the relationships between these galaxies, we will leave that for future work and in the present paper focus on the demographics to provide insight into the dominant timescales associated with environmental quenching.

### Table 3. Spectral index measurements are shown for median combined spectra of each population type. The \(H\delta\) and [OII] indices are rest-frame equivalent widths, measured in \(\AA\), defined such that they are positive in absorption for \(H\delta\), and positive in emission for [OII]. Uncertainties are 68 per cent confidence limits obtained by Monte-Carlo resampling the measurements assuming the uncertainties on each spectral pixel are Gaussian distributed.

| Index | \(D4000\) | \(H\delta\) \((\AA)\) | \([\text{[OII]}]\) \((\AA)\) |
|-------|-----------|-----------------|----------------|
| Cluster |
| GV    | \(1.5 \pm 0.1\) | \(4.1^{+4.2}_{-4.4}\) | \(4.0^{+2.8}_{-2.6}\) |
| BQ    | \(1.52 \pm 0.04\) | \(4.8 \pm 1.2\) | \(0.76 \pm 1.6\) |
| PSB   | \(1.34 \pm 0.04\) | \(3.7^{+1.3}_{-1.5}\) | \(2.1^{+1.6}_{-1.7}\) |
| Field |
| GV    | \(1.40 \pm 0.05\) | \(3.1 \pm 1.3\) | \(10.7^{+3.8}_{-2.1}\) |
| BQ    | \(1.39 \pm 0.05\) | \(4.6^{+1.3}_{-1.4}\) | \(7.4^{+3.0}_{-2.7}\) |
| PSB   | \(1.3 \pm 0.1\) | \(1.8^{+5.3}_{-5.1}\) | \(2.1^{+5.0}_{-5.2}\) |

The PSB galaxies overlap substantially with the BQ population and the blue end of the GV in both colour-colour diagrams, but they also extend into the Q domain. Interestingly, Figure 3 shows that both the BQ and GV galaxies typically have large D4000 break strengths characteristic of old populations, and larger than the threshold used to define PSB galaxies, despite their blue \((U - V)\) colours.

We compare the average of the available spectra for cluster members of each galaxy type, in Figure 4. The spectra are normalized...
normalized by the volume of the survey between $1 < z < 1.5$. We do not include the PSB population here, because they are drawn from the spectroscopic sample where large and uncertain completeness corrections are required; we will consider their relative abundance subsequently. Finally, as stated in § 2.2.1, we do not exclude BCGs from this analysis.

The binned data are fit with Schechter functions of the form

$$\phi(M)dM = \frac{dN}{dM}dM = \phi^* \left( \frac{M}{M^*} \right)^\alpha \exp\left( -\frac{M}{M^*} \right) dM. \quad (2)$$

or, for $x = \log_{10} M/M_\odot$ as plotted in the Figure,

$$\phi(x)dx = \frac{dN}{dx}dx = \ln 10 \left( \frac{dN}{dM} \right) Mdx = \ln 10 \phi^* M^* \left( \frac{M}{M^*} \right)^{1+\alpha} \exp\left( -\frac{M}{M^*} \right) dx. \quad (3)$$

Following van der Burg et al. (2020) we only fit the data with $M > 10^{9.2} M_\odot$, as the completeness corrections are both large and systematically uncertain (due in part to sparse and biased spectroscopic sampling) below that limit. The normalization parameter is fixed by forcing the integral to match the sum of the data where $\log(M/M_\odot) \geq 9.7$; the other two parameters are fit by minimizing the $\chi^2$ statistic. There are six data bins, omitting the lowest mass point, and two parameters, for $\nu = 4$ degrees of freedom.

The resulting fit parameters are given in Table 4 and we show the 68 per cent confidence ranges of $M^*$ and $\alpha$ in Figure 6. These are compared with the SMF fit parameters of van der Burg et al. (2020), which were based on a different classification, using $UVJ$ colours, and only separated galaxies into two types: quiescent and star-forming. For the total cluster sample, as well as the Q population, the fit parameters we derive are fully consistent with those of van der

3 van der Burg et al. (2020) fit the data for the SF population to a lower stellar mass limit, of $M > 10^{8.2} M_\odot$. As the fit parameters are sensitive to the mass limit chosen, we elect to fit all our populations over the same, conservative, mass range.

4 For cases where the best fit has $\chi^2/\nu > 1$, we temporarily increase the error bars to achieve $\chi^2 = 1$ and then find the 68 per cent confidence range.

Table 4. The values for the two-parameter Schechter mass function fits, for each of the galaxy populations in both the cluster and the field. The values in this table correspond to the parameters in Equation 2, and are used to plot the SMF fits shown in Figure 5. For the cluster, the units of $\phi^*$ are $10^{-15} \text{Mpc}^{-3} \text{dex}^{-1}$, while for the field they are $10^{-15} \text{Mpc}^{-3} \text{dex}^{-1}$. The $\chi^2$ values are calculated for six data points (the lowest mass bin is excluded from the fit) and two parameters (the normalization is fixed), yielding 4 degrees of freedom.

|       | $\chi^2$ | $\log_{10}(M^*/M_\odot)$ | $\alpha$ | $\phi^*$ |
|-------|---------|--------------------------|---------|--------|
| Cluster |         |                          |         |        |
| SF    | 1.1     | 10.53                    | -0.69   | 7.0    |
| Q     | 5.4     | 10.80                    | -0.26   | 6.4    |
| GV    | 1.4     | 10.77                    | -0.66   | 1.3    |
| Total | 6.0     | 10.82                    | -0.64   | 8.8    |
| Field  |         |                          |         |        |
| SF    | 1.6     | 10.80                    | -1.31   | 13.4   |
| Q     | 5.3     | 10.72                    | -0.28   | 15.6   |
| GV    | 1.3     | 10.80                    | -0.63   | 5.5    |
| Total | 10.7    | 10.89                    | -1.13   | 19.5   |

Burg et al. (2020). For the SF galaxies we find a somewhat larger $\alpha$ and smaller $M^*$. For the field sample, the fit parameters for the total, Q and SF populations are in excellent agreement with van der Burg et al. (2020), who used the independent, larger UltraVISTA (Muzzin et al. 2013) survey.

In both the cluster and field environments, the shape of the GV SMF is intermediate between that of the SF and Q galaxies. Though the parameters are not tightly constrained, they are inconsistent with the SF population fit. It is therefore unlikely that the majority of this intermediate population can be made up of galaxies transformed directly from the infalling SF population, without a significant change in stellar mass. On the other hand, the SMF of cluster BQ galaxies is fully consistent with that of the SF galaxies (Figure 6). Though the fit is not well constrained, particularly in the field, due to the small sample size, the fit parameters are highly inconsistent with

5 This difference is due primarily to the fact that we only fit the data above $M > 10^{9.2} M_\odot$, while van der Burg et al. (2020) include data above $M > 10^{9.2} M_\odot$ when fitting the SF population.
Figure 6. We show the 68 per cent confidence limits on the $M^*$ and $\alpha$ parameters of our Schechter function fits, for the total (black) quiescent (red), star-forming (blue), green-valley (green) and blue quiescent (orange) galaxies. The white dots represent the best fit. Parameters for the cluster population are shown in the Left panel, and parameters for the field population are on the Right panel. The crosses are the best fit parameters to the total, quiescent and star-forming populations (defined in $U V J$ space, without a green valley) by van der Burg et al. (2020); open ellipses indicate their 1 $\sigma$ confidence ranges. The parameters of the BQ population are not well constrained and the 68 per cent confidence limit extends beyond the limits of this figure.

those of the Q population. This, together with their rarity in the field population discussed below, supports an interpretation in which most of the cluster BQ galaxies arise from rapid quenching of the SF galaxies after infall into the cluster environment.

Throughout the rest of this paper we represent the SMF of each population as $\phi^i_j$, where $i \in \{SF, GV, Q, BQ\}$ represents the subpopulation type, and $j \in \{C, F\}$ identifies the environment as cluster or field. The total SMF in each environment is just written as $\phi^C$ or $\phi^F$, with no subscript. Normalizing the SMF for each of the populations by the total SMF in the relevant environment converts the $\phi^i_j$ into fractions $f^i_j$, which allows us to compare the cluster and field distributions independently of any overall difference in SMF shape.

3.3 Population abundance distributions

3.3.1 Stellar mass dependence

In Figure 7 we show the abundance of each subpopulation as a fraction of the total, in bins of stellar mass, for the cluster and field environments. Uncertainties, here and elsewhere in the paper, are obtained from 1000 Monte Carlo samples of our galaxy populations and represent the 68 per cent confidence intervals. We include the spectroscopic PSB sample here (recall that the BQ and PSB galaxies are not independent of the other three classifications). As the spectroscopy is unbiased with respect to type for galaxies $M \gtrsim 10^{10.2} M_\odot$ (Balogh et al. 2021), the relative PSB abundance in bins of stellar mass is robust. Below this mass limit the spectroscopic sample is incomplete, and the ratios should be used with caution. The photometric sample of SF, Q, GV and BQ galaxies are representative down to $M \approx 10^{9.5} M_\odot$, though we caution that the lowest mass bin has large and uncertain completeness corrections (and hence was excluded from the SMF fits).

The BQ galaxies exhibit a strong correlation with stellar mass, their relative abundance increasing toward lower masses. This closely parallels the trend seen in the SF galaxies, as expected given the similarity in their SMF shapes. The cluster PSB sample also shows a similar behaviour, though the uncertainties are considerably larger. This suggests that their SMF is also similar in shape to that of the BQ and SF galaxies, and is consistent with a scenario in which they arise from approximately mass-independent quenching of the infalling SF galaxies. The GV galaxies, on the other hand, show a more modest trend with mass in the cluster environment. All three cluster transition populations show a drop in abundance in the lowest stellar mass bin, but this should be treated with caution given the relatively large and uncertain incompleteness and cluster membership corrections\(^6\) at this mass. In the field, both the GV and PSB populations show a decreasing fraction with decreasing mass, opposite to what is observed in the cluster environment, and suggesting that they may have a physically distinct origin. We note here also that the abundance of massive ($M > 10^{10.8} M_\odot$) BQ galaxies in the field, $(1.4 \pm 1) \times 10^{-5}$ Mpc\(^{-3}\), is in agreement with the $(0.9 \pm 0.1) \times 10^{-5}$ measured by Belli et al. (2019) at the same redshift, and corresponds to 1.8 per cent of the total.

The most significant, and well-known, difference in cluster galaxy populations is the excess abundance of Q galaxies, and corresponding lack of SF galaxies, as seen in Figure 7. This can be characterized by a "Quenched Fraction Excess"\(^7\) (QFE; e.g. van den Bosch et al. 2008; Peng et al. 2010; Bahé et al. 2017; van der Burg et al. 2020) given by:

$$QFE \equiv \frac{f^C_{SF} - f^C_{Q}}{f^F_{SF}}, \quad (4)$$

which represents the fraction of field SF galaxies at the epoch of observation that need to be quenched to represent their abundance in clusters at the same time. By comparing the field and cluster at

\(^6\) Specifically, at these masses the SF galaxies are the dominant population, and the contamination from field galaxies in the cluster sample is high, leading to a large correction. An overestimate of the cluster SF population in this bin would lead to underestimates of the GV, BQ and PSB fractions relative to the total.

\(^7\) We adopt this terminology as the most accurate description of the quantity, following Wetzel et al. (2012); Bahé et al. (2017); van der Burg et al. (2020); Reeves et al. (2021). Similar definitions in the literature refer to this quantity as the "transition fraction" (van den Bosch et al. 2008), "conversion fraction" (Balogh et al. 2016; Fossati et al. 2017), and "environmental quenching efficiency" (Peng et al. 2010; Wetzel et al. 2015; Nantais et al. 2017; van der Burg et al. 2018).
the same redshift, this measures the quenching that needs to occur for reasons that are correlated with environment, over and above the "natural" evolution of field galaxies. We show the QFE as a function of stellar mass in Figure 8, both using the binned data and the smooth Schechter function fits to the SMFs. We also compare with the analysis of van der Burg et al. (2020), who used the same cluster data but a different galaxy classification and an independent field sample taken from UltraVISTA (Muzzin et al. 2013). Despite these differences, our measurements are in good agreement with theirs.

As observed by others (e.g. Balogh et al. 2016; Kawinwanichakij et al. 2017; van der Burg et al. 2020), the QFE increases steadily with stellar mass, though we note that over the substantial mass range $10^{9.75} < M/M_\odot < 10^{11}$, the data are consistent with a mass-independent $QFE \sim 0.4$. It is also remarkable that this value of 0.4 agrees very well with the QFE measured at low redshift for all satellite galaxies (Peng et al. 2012).

In Figure 9 we show the difference in the fraction of each candidate transition galaxy type in the cluster, relative to the field, as a function of stellar mass. For all three populations, this difference is consistent with zero for galaxies with $M > 10^{10.5} M_\odot$, but increases with decreasing stellar mass, reaching $\sim 10$ per cent at $M \approx 10^{9.5} M_\odot$.

### 3.3.2 Clustercentric radius variations

Figure 10 shows how the fraction of galaxies in each population varies with distance from the cluster centre, and how this compares with the corresponding fraction in the field. These fractions again include all galaxies with $M > 10^{10.5} M_\odot$, with completeness weights applied to the photometric samples as described in § 2.2. The PSB population includes galaxies below the spectroscopic completeness limit and we apply no corrections; therefore these values are not necessarily representative of a mass-limited sample. As expected, we see an increase in star-forming galaxies with radius, and a decrease in the fraction of quiescent galaxies. Overall the cluster population shows a highly significant excess of quiescent galaxies, and a corresponding deficit of star-forming galaxies, relative to the field.

All three transition populations have an abundance of about ten per cent in the cluster environment, with at most modest dependence on distance from the centre. As noted above, the field fraction of BQ galaxies we measure is consistent with what Belli et al. (2019) find at similar redshifts (at least for the most massive galaxies), and significantly lower than what we observe in the cluster population. However, the fraction of field PSB galaxies is higher than the ~ 3 per

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**Figure 7.** Left: The abundance of each cluster population, relative to the total, is shown as a function of stellar mass. For the SF, Q, BQ and GV galaxies, this is measured from the SMFs presented in Figure 5. For the spectroscopic PSB galaxies we show the fraction of spectroscopically confirmed PSB cluster members relative to the total sample of spectroscopic cluster members; these values should be treated with caution for $M < 10^{10.2} M_\odot$, as the spectroscopic sample is not unbiased at those masses. The GV and PSB populations are not independent of the other three, so the fractions do not sum to unity in a given bin. Right: The same, but for the field population. For the photometric sample, this is all galaxies $\geq 1.5$ Mpc from the cluster centre, in the redshift range $1 < z < 1.5$. For the PSB population we take all spectroscopic non-cluster members, also at $1 < z < 1.5$, as determined by Biviano et al. (2021). Small offsets in the plotted $x$–position for the BQ and GV points are applied for clarity.

**Figure 8.** The QFE (Equation 4) is shown as a function of stellar mass, based on the measured SMFs of the star-forming galaxies in the cluster and field sample. Black points represent the binned data as medians with 68 per cent confidence limit error bars. The measurement inferred from the Schechter function fits is shown as the red line for the best-fit parameters, and the grey confidence limit error bars. The measurement inferred from the Schechter function of stellar mass in Figure 8, both using the binned data and the "natural" evolution of field galaxies. We also show the QFE as a function of stellar mass in Figure 8, both using the binned data and the smooth Schechter function fits to the SMFs. We also compare with the analysis of van der Burg et al. (2020), who used the same cluster data but a different galaxy classification and an independent field sample taken from UltraVISTA (Muzzin et al. 2013). Despite these differences, our measurements are in good agreement with theirs. As observed by others (e.g. Balogh et al. 2016; Kawinwanichakij et al. 2017; van der Burg et al. 2020), the QFE increases steadily with stellar mass, though we note that over the substantial mass range $10^{9.75} < M/M_\odot < 10^{11}$, the data are consistent with a mass-independent $QFE \sim 0.4$. It is also remarkable that this value of 0.4 agrees very well with the QFE measured at low redshift for all satellite galaxies (Peng et al. 2012).

In Figure 9 we show the difference in the fraction of each candidate transition galaxy type in the cluster, relative to the field, as a function of stellar mass. For all three populations, this difference is consistent with zero for galaxies with $M > 10^{10.5} M_\odot$, but increases with decreasing stellar mass, reaching ~ 10 per cent at $M \approx 10^{9.5} M_\odot$. For the PSB population we take all spectroscopic non-cluster members, also at $1 < z < 1.5$, as determined by Biviano et al. (2021). Small offsets in the plotted $x$–position for the BQ and GV points are applied for clarity.
cent measured by both Muzzin et al. (2012) and Yan et al. (2009b) at comparable redshifts. This results in a less significant difference between the cluster and field fractions. Although the overall fractions of transition galaxies do not show a strong trend with environment, their abundance relative to the SF population does strongly increase toward the cluster centre, as the latter population shows a strong radial trend. Whether or not there is an environmental signature, therefore, depends on what is assumed about the parent population, a point that we will address in § 4.1.

3.3.3 Phase space distribution

For the spectroscopic sample we have radial velocity information, so we can also consider their distribution in position-velocity “phase space”, shown in Figure 11. A similar analysis was done for PSB galaxies in the GCLASS sample of clusters, at slightly lower redshift, by Muzzin et al. (2014). Here we aim to compare directly with galaxies in the GCLASS sample of clusters, at slightly lower redshift, “space”, shown in Figure 11. A similar analysis was done for PSB galaxies with $M > 10^{10.5} M_\odot$, and spectroscopic redshifts in phase space, as defined by Muzzin et al. (2014). The solid contours represent the same phase space bins adopted by Muzzin et al. (2014).

Figure 9. We show the difference in the abundance of candidate transition galaxies in clusters, relative to the field, as a function of stellar mass. Points show the median with 68 per cent confidence limit error bars, and the corresponding Schechter function fits to the GV and BQ SMFs are shown as solid lines with a shaded region for the 68 per cent confidence limits. The horizontal, dashed line indicates identical abundances in both environments. The PSB and BQ points are shifted slightly in the horizontal direction for clarity only.

Figure 10. The relative abundances of each galaxy population considered in this paper are shown as a function of clustercentric distance. The comparison field is shown as the bars on the right, and includes all the galaxies at $1 < z < 1.5$ beyond 1.5 Mpc. The height of the bars represents the 1σ uncertainty on the fractions. For the PSBs the plotted fraction is their abundance relative to the total spectroscopic sample, limited to $M > 10^{9.5} M_\odot$. This is well below the spectroscopic completeness limit, and no completeness corrections are applied. For all the other populations the fraction is relative to the total photometric sample, completeness corrected to $M > 10^{9.5} M_\odot$. The PSB and BQ populations are not independent of the other three, so the fractions do not add to unity in a given bin.

Figure 11. The distribution of galaxies with $M > 10^{10.2} M_\odot$ and spectroscopic redshifts in phase space, as defined by Muzzin et al. (2014). The solid contours represent the same phase space bins adopted by Muzzin et al. (2014).

4 DISCUSSION

We have shown that all three transition populations — GV, BQ and PSB — are modestly overabundant in clusters, only for low mass galaxies with $M < 10^{10.5} M_\odot$. It is remarkable in particular that the excess of the GV population is not larger than that of the BQ or PSB galaxies, which require relatively rapid quenching on a timescale < 1 Gyr. Since the GV will capture all transitions, whether slow or fast, this result implies that most of the cluster-driven transformation may in fact be via the fast-quenching mode described by Belli et al. (2019), leading to a BQ and PSB appearance. In this section we attempt to quantify this further by estimating the timescales associated with each of these populations, and then discuss the implications in the broader context of galaxy evolution. The quantities we use here to link the transition galaxy populations with a quenching timescale...
require a number of assumptions and simplifications, and are derived in Appendix A.

4.1 Transition Timescales

The excess abundance of transition galaxies is related to both the rate of environmental quenching, and the time spent in that phase. As derived in Appendix A.1.2, for a given transition population \( i \) we can write

\[
R_i \tau_i = f_i^C - f_i^F, \tag{5}
\]

where \( R_i \) is the fraction of infalling field SF galaxies that are quenched per unit time, and \( \tau_i \) is the time spent in the transition phase \( i \). This requires a number of assumptions, including that the mass accretion rate of the cluster is constant with time, the excess abundance is due only to quenching (and not, for example, rejuvenation of quiescent galaxies), and that the number of transition galaxies arising due to non-environmental reasons is proportional to the total galaxy population. Results corresponding to an alternative choice for the latter assumption are presented in Appendix A1.1. We show \( R_i \tau_i \) as a function of stellar mass for the GV population in Figure 12. As expected given the results shown in Figure 9, the data are consistent with \( R_{GV} \tau_{GV} = 0 \) for all stellar masses, apart from one bin. For the low mass galaxies \( M < 10^{10.5} \odot \) we find a 1σ upper limit of \( R_{GV} \tau_{GV} < 0.03 \). Note that the fit to the data shows a more significant detection, as the lowest mass bin was not included in the fit to the SMFs, as described in § 3.2. Values of \( R_i \tau_i < 0 \) are permitted, and correspond to the case where there are relatively more transition galaxies in the field than the cluster population. Such values point to limitations in the simple model (for example, neglecting mergers and tidal disruption of galaxies), but we note that we do not measure a statistically significant negative value in any bin.

From analysis of the spectra of both BQ (Bell et al. 2019) and PSB (Muzzin et al. 2012; French et al. 2018) galaxies it has been argued that their lifetimes are \( \tau \sim 0.5 \pm 0.3 \) Gyr. If we adopt this timescale (neglecting the large uncertainty for the moment) we can estimate the effective quenching rate \( R \) over that time from Equation 5. These rates are shown, as a function of stellar mass, in Figure 13. The uncertainties are too large to permit strong conclusions, even before considering the additional uncertainty in assumed timescale \( \tau \). But both populations yield similar results and are consistent with a quenching rate at the epoch of observation that is significantly greater than zero, and consistent with each other to within a factor of two, for low mass galaxies. The median value for the low mass
for the PSB galaxies we find $R_{PSB} = 0.09 \pm 0.07 \text{ Gyr}^{-1}$, though we remind the reader that the spectroscopic sample on which this is based is not representative of all galaxy types for $M < 10^{10.2} \text{ M}_\odot$. Adopting a longer (shorter) timescale $\tau_I > 0.5$ would reduce (increase) these rates proportionally.

As the data only constrain the combination $R_T \tau_I$, we cannot determine timescales $\tau_I$ directly without an assumption about $R_T$. Under the assumption that the three populations are different phases of the same quenching process, then their corresponding rates should be equal, $R_{BQ} = R_{PSB} = R_{GV}$. In this case we can calculate their relative timescales. We show the GV and PSB timescales relative to that of the BQ population, in Figure 14. We choose the BQ as the reference population because it yields the best constraints on $R_T \tau_I$, due to its relatively large sample size (compared with the spectroscopic PSB sample) and its contrast with the field (compared with the GV galaxies). From this we conclude that, for low mass galaxies, the lifetimes in the PSB and GV phase are consistent with the lifetime of the BQ phase. If anything, the GV abundance requires an even shorter life-time, $\tau_{GV} = (0.3 \pm 0.3) \text{ Gyr}$, suggesting that slow-quenching through the green valley is not a dominant mode for environmental transformation. For example, the slow quenching model of Belli et al. (2019) predicts $UVJ$ colours that are consistent with our GV definition for $\sim 1 \text{ Gyr}$ (comparing their Figure 12 with the right panel of our Figure 1). This does not, however, rule out the possibility of a long delay time between when a galaxy first enters a dense environment and when quenching begins (e.g. Wetzel et al. 2012; De Lucia et al. 2012; Mok et al. 2014; McGee et al. 2014; Foltz et al. 2018). From an analysis of the SF population in GOGREEN, Old et al. (2020) measured a small but significant difference in the SFRs of cluster galaxies relative to the field, in the sense that low mass cluster SFRs are lower by about 50 per cent. As these galaxies are independent of the transition galaxies studied here, this implies that there is a modest environmental effect present prior to the rapid transition through the GV/BQ/PSB phase, as observed at lower redshift (e.g. Vulcani et al. 2010; Haines et al. 2015; Finn et al. 2018).

4.2 The evolution of cluster galaxy quenching

It is notable that the QFE we (and van der Burg et al. 2020) measure, $\sim 0.4$, is very similar to what is measured at $z \sim 0$ (Peng et al. 2012; Omand et al. 2014) and at $0.4 < z < 0.8$ (Poggianti et al. 2009) for similar environments. Given the shorter age of the Universe at $z = 1$, we show in Appendix A that a time independent QFE implies (under several assumptions) that the quenching rate must decrease with time as $R \propto t^{-1}$, and consequently $R = T \times QFE$, where $T$ is the lifetime of the cluster at a given epoch.

We can therefore use observations of post-starburst galaxies in clusters at different redshifts to estimate the evolution of $R$ directly from Equation 5, and compare this with the predicted evolution assuming a constant QFE. This is shown in Figure 15, where we compare our results with the abundance of spectroscopic PSB in massive clusters observed at $z \sim 0$ from (Zabludoff et al. 1996) and Paccagnella et al. (2019), and at intermediate redshifts from Poggianti et al. (2009), assuming $\tau = 0.5 \text{ Gyr}$ is constant. The literature values are based on the fraction of PSB galaxies relative to the total population in luminosity-limited samples that are comparable to the stellar mass limit of the present work, though not precisely matched\(^8\).

\[^8\] Given the strong mass-dependence we find, a more careful analysis in future work is warranted.

For GOGREEN, the data point shown is based on the BQ population, as this is complete to lower masses than the spectroscopic PSB sample, but implies rates that are consistent with those obtained from the PSB, with smaller uncertainties. The data show a modest evolution of $R$ over $0 < z < 1.2$, strongest when compared with the low fraction of PSB observed by Zabludoff et al. (1996) at $z \sim 0$ (see also Hogg et al. 2006; Vulcani et al. 2015). This is compared with the expected evolution implied by a constant QFE, $R = T \times QFE$ where $T$ is computed assuming a formation redshift $z_f = 3$. Given the substantial statistical and systematic uncertainties, the data are consistent with this simple model, and hence with the observation that QFE is constant. We also compare with the evolution of the inverse of the dynamical time, which has similar behaviour that is indistinguishable given these data.

Analysing the same GOGREEN clusters, with the same data, van der Burg et al. (2020) showed that the shape of the quiescent galaxy SMF is identical in the cluster and field environments. This is significantly different from what is found at low redshift (e.g. Baldry et al. 2006; Peng et al. 2012), where the low-mass end of the quiescent SMF in clusters rises steeply with decreasing mass, as would be expected if SF galaxies accreted from the field were being quenched independently of their stellar mass. In particular, van der Burg et al. (2020) showed that the shape of the cluster quiescent SMF cannot be reproduced simply by adding a mass-independent fraction $f$ of field SF galaxies to the quiescent population, as:

$$\phi_Q^C(M) = A \left( \phi_Q^F(M) + f \phi_S^F(M) \right),$$

where $A$ is a renormalization constant. In Appendix A1.1 we show that Equation 6 holds if $f$ is a function of mass. Specifically, $f(M)$ can be related to the QFE and to the relative shapes of the total SMFs, as:

$$f(M) = \xi(M)QFE(M) + \frac{\phi_S^F(M)}{\phi_Q^F(M)} [\xi(M) - 1],$$

where $\xi(M) = \phi_C(M)/A\phi_Q^F(M)$. Note that $f \neq QFE$ unless the total SMF in the cluster and field have the same shape, so that $\phi_C = A\phi_Q^F$. Instead we obtain two terms. The first is due to converting SF galaxies to Q, and characterised by the QFE. The second term results...
We find that from needing to add an excess of both SF and Q galaxies from the field only, as the shaded region. through merging of lower mass galaxies, or preferential accretion of not enough of them. There must be an additional source, for example through merging of lower mass galaxies, or preferential accretion of massive galaxies.

We can compare this constraint on \( f(M) \) with independent predictions of the QFE, via the quenching rate \( R \) derived from the BQ galaxy abundance. This depends on the BQ lifetime, and we will show the results assuming both \( \tau_{BQ} = 0.5 \) Gyr and \( \tau_{BQ} = 1.0 \) Gyr. From this we can predict the first term in Equation A21 for \( f(M) \), again assuming \( R T \times QFE \), and a term redshift \( z_f = 3 \). The result is shown as the orange curves in Figure 16. At the high mass end the shape is dominated by the second term in Equation A21, that is independent of quenching and hence the BQ constraints. The predicted curve has a similar shape to the data, but lies below it. This difference reflects our observation that the QFE inferred from the SMFs is large at these masses, yet we measure no significant excess of transition galaxies, with the shallow slope of the quiescent SMF in clusters that drives the low \( f(M) \) in Figure 16. The fact that the SMF of the BQ population (and, indirectly, the PSB population) looks similar to that of SF galaxies in the field further reinforces that we would expect to see an excess of low mass galaxies in the quiescent SMF, that does not appear to be there.

In another work studying these same clusters, Webb et al. (2020) found that the mass-weighted ages of cluster and field quiescent galaxies are comparable; if anything, cluster galaxies are somewhat older. This is not what would be expected if cluster galaxies were first quenched upon infall, as these environments would then host quiescent galaxies that are younger than those in the field (e.g. Muzzin et al. 2012). A proposed interpretation is that “pre-processing” is important; i.e. environmental quenching is initiated when galaxies first become satellites, long before they are accreted into more massive clusters. Analysis of GOGREEN systems as a function of halo mass supports this interpretation for massive galaxies (Reeves et al. 2021), as does a recent analysis of galaxies in the infall regions of these same clusters (Werner et al. submitted). These observations, together with the older ages measured by Webb et al. (2020) and our results here showing no significant excess of transition galaxies for massive galaxies, all point to the need for these galaxies to have ended their star formation at \( z > 2 \), possibly in a protocluster environment, and that accretion onto the existing cluster at \( z \sim 1 \) plays little or no role in further star formation quenching.

The picture is a little less clear for the lower mass galaxies. Here, the abundance of transition galaxies is enough to fully explain the QFE under simple assumptions, suggesting that accretion-driven quenching is the dominant route for forming quiescent galaxies. This is consistent with the work of (Reeves et al. 2021) and Werner et al. (submitted), which indicate little or no pre-processing in this mass regime. It is in some tension with the shape of the quiescent SMF (Figure 16), and the small age difference of \( 0.1^{+0.46}_{-0.31} \) Gyr between cluster and field quiescent galaxies found by Webb et al. (2020). However, the statistical and systematic uncertainties in both cases are large enough that we cannot rule out a simple interpretation where accretion-driven quenching plays an important or even dominant role for creating low mass, quiescent galaxies in clusters at \( z \sim 1 \). Further insight will be gained from a careful study of how the SMFs of these different populations depend on halo mass and redshift (e.g. Wild et al. 2020; Scolovsly et al. 2018). Moreover, observations of protoclusters at \( z \gtrsim 2 \) will help to determine the “initial conditions” of the cluster population, to disentangle accretion-driven quenching from differences that arise in the early cluster formation phase.

5 CONCLUSIONS

We have taken advantage of deep rest-frame NUV photometry in the GOGREEN sample of \( 1 < z < 1.5 \) galaxy clusters to identify transition galaxies in the green valley (GV) between the dominant star-forming and quiescent populations. This definition has the advantage of being complete, in the sense that it is certain to include every galaxy that transitions from the star-forming to quiescent population, at some point during its evolution. We compare this population with two other definitions of transition galaxies - blue quiescent (BQ) galaxies and spectroscopically identified post-starburst (PSB) galaxies. These have the advantage that they are likely more pure, in the sense that a larger fraction of the sample are expected to be in the process of rapidly quenching their star formation. They may be incomplete, as it is possible for galaxies to transition without...
passing through either of these phases. Our main observations are summarized as follows:

- The SMF of GV galaxies has a shape most similar to that of the Q population, and inconsistent with that of the star-forming (SF) galaxies. The opposite is true of the BQ galaxies. Cluster BQ galaxies have strong Hδ absorption in their spectra, 5 ± 1 Å equivalent widths, comparable to that of the PSB galaxies. The three transition populations partially overlap in colours and D4000 break strength, but are substantially independent. They may sample different phases of evolution during the final quenching of star formation, or different pathways taken by different galaxies depending on their dust evolution and past star formation history.
- For massive galaxies, \( M > 10^{10.5} M_\odot \), we find no significant difference in the fraction of PSB, BQ or GV galaxies in clusters, compared with the field.
- For low stellar masses \( M < 10^{10.5} M_\odot \), BQ, PSB and GV galaxies make up a ~ 5−10 per cent greater proportion of the cluster population than in the field.
- We do not find a strong radial or phase space dependence on the distribution of transition galaxies relative to the total population. Relative to the SF population, all three populations are significantly more abundant in the central regions of the cluster.
- Assuming the PSB and BQ phases last for ~ 0.5 Gyr, as argued by others based on their spectra (Belli et al. 2019; Muzzin et al. 2014; French et al. 2018), their abundances imply that 20–30 per cent of infalling SF galaxies with \( M < 10^{10.5} M_\odot \) are quenched every Gyr.
- The relative abundance of GV galaxies implies environmentally quenched galaxies exist in this phase for a comparable or even shorter time than in the BQ phase.

We conclude that the BQ population is the best tracer of recent environmental quenching, as it i) can be identified photometrically; ii) exhibits the largest excess abundance in clusters, relative to the field; iii) has a SMF consistent with the SF population, and average spectra that are most similar to classic post-starburst spectra, with strong Hδ absorption; and iv) appears to capture most, if not all, of the environmentally quenching galaxies at some point in their lifetime. The GV, on the other hand, shows at most a modest excess abundance in clusters relative to the field, and appears to be the most heterogeneous, with environmentally quenching galaxies comprising less than half the cluster population.

Our results are consistent with a fairly simple picture that is qualitatively different for high and low mass galaxies. For massive galaxies, \( M > 10^{10.5} M_\odot \), we do not find a significant excess of any type of transition galaxy – GV, BQ or PSB – in clusters. Though the uncertainties are too large to draw strong conclusions, the results are consistent with most massive cluster quiescent galaxies being quenched before accretion on to the cluster, via pre-processing in group or protocluster environments (Reeves et al. 2021, Werner et al., submitted). For lower mass galaxies, \( M < 10^{10.5} M_\odot \), the excess of GV, PSB and BQ galaxies all indicate that approximately 20–30 per cent of the star-forming cluster population is quenched every 1 Gyr, in excess of what would be expected in the field. The final quenching process itself is rapid (\( \tau < 1 \) Gyr), and most quenching galaxies pass rapidly through the GV and go through both a PSB phase (with blue colours but no nebular emission) and a BQ phase (at the blue end of the quiescent region of the UVJ diagram). The inferred quenching rate is consistent with the observed QFE at both \( z = 1 \) and \( z = 0 \), implying that this rapid quenching can account for most of the low mass excess quiescent population in clusters. This does not exclude a longer delay time preceding the final quenching, that can lead to a modest reduction in SFR (e.g. Old et al. 2020) prior to the rapid transition. We conclude therefore that most \( M < 10^{10.5} M_\odot \) quiescent galaxies were quenched upon infall into the cluster.
DATA AVAILABILITY

All data used in this paper are available from the GOGREEN and GCLASS public data release, at the CADC (https://www.cadc-ccda.hia-iha.nrc-cnrc.gc.ca/en/community/gogreen), and NSF’s NOIR-Lab (https://datalab.noao.edu/gogreendr1/).

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APPENDIX A: QUENCHED FRACTION EXCESS AND TRANSITION RATES

Here we consider how the Quenched Fraction Excess (QFE, Equation 4) can be related to the instantaneous quenching rate of infalling galaxies. In particular, we are looking for some insight into the observation that QFE at fixed stellar mass and environment has been approximately constant, over the past 9 Gyr. We will demonstrate that QFE can be linked to a quenching rate as we have assumed in this paper, but that it requires several strong assumptions. Furthermore, the interpretation is not unique, and we briefly demonstrate two other models for producing an excess of quenched galaxies that can lead to a constant QFE.

As in the main body of the paper, we use \( \phi_i^{SF} \) to represent the stellar mass function of population \( i \in \{SF, Q, PSB, GV, \ldots \} \) in environment \( j \in \{C, F\} \) for cluster or field. The total SMF in each environment is written without a subscript, \( \phi^{C} \) and \( \phi^{F} \). Finally we write the fraction of galaxies in population \( i \) and environment \( j \) as \( f_i^j = \phi_i^{SF} / \phi_i^{C} \).
The \( \phi_C^F(M, T) \) in the integrand is always evaluated at the same mass \( M \) corresponding to \( \phi_{S,F}(M) \) on the left hand side: \( \gamma \phi_{S,F}(M)dt \) is therefore the number of galaxies at final mass \( M \) that were accreted in that time interval, whatever their actual mass at earlier time \( t \). Here and below we are making a strong (and almost certainly incorrect) assumption that the quenching rate \( \mathcal{R} \) depends only on the final mass \( M \) of a galaxy. In what follows we drop the explicit \( M \) dependence to make the formulas more concise.

The total number of quenched cluster galaxies is given by the sum of the environmentally quenched and self-quenched populations:

\[
\phi^C_Q = \phi^C_{Q,env} + \phi^C_{Q,s}.
\]

(A4)

Expanding the first term on the right hand side we get

\[
\phi^C_Q = \int_0^T \phi_{S,\mathcal{R}} dt + \phi^C_{Q,s}
\]

(A5)

\[
\approx \int_0^T \gamma(t) \phi_{S,F}^C \mathcal{R}(t) dt + \phi^C_{Q,s}
\]

(A6)

\[
\approx \gamma \phi_{SF}^C \int_0^T \mathcal{R}(t) dt + \phi^C_{Q,s}
\]

(A7)

Now we assume the fraction of self-quenched galaxies is the same in the cluster and field, so

\[
\frac{\phi^C_{Q,s}}{\phi^C} = \phi^C_{Q,F}
\]

(A8)

and

\[
\phi^C_Q \approx \gamma \phi_{SF}^C \int_0^T \mathcal{R}(t) dt + \phi^C_{Q,F} \frac{\phi^C}{\phi^F}.
\]

Divide both sides by \( \phi^F \) to get

\[
\frac{\phi^C_Q}{\phi^F} \approx \gamma \frac{\phi_{SF}^C}{\phi^F} \int_0^T \mathcal{R}(t) dt + \phi^C_{Q,F} \frac{\phi^C}{\phi^F}.
\]

(A9)

Using \( \gamma \) from Equation A2, we obtain

\[
\frac{\phi^C_Q}{\phi^F} \approx \frac{1}{T} \frac{\phi^C_{SF}}{\phi^F} \int_0^T \mathcal{R}(t) dt + \phi^C_{Q,F} \frac{\phi^C}{\phi^F}
\]

or

\[
\phi^C_Q \approx \frac{1}{T} \frac{\phi^C_{SF}}{\phi^F} \int_0^T \mathcal{R}(t) dt + \phi^C_{Q,F}.
\]

(A10)

This can be rearranged to give the QFE:

\[
QFE = \frac{\phi^C_Q - \phi^C_{Q,F}}{\phi^C_{SF}} \approx \frac{1}{T} \int_0^T \mathcal{R}(t) dt.
\]

(A13)

In this case, a constant \( QFE \) means \( \mathcal{R} \propto t^{-1} \) and

\[
\mathcal{R} \propto \frac{QFE}{T}.
\]

(A14)

On the other hand, if the quenching rate \( \mathcal{R} \) is constant, then

\[
QFE \approx \frac{RT}{2}
\]

(15)

should grow with time. This yields a simple, and intuitive relationship between \( QFE \) and \( \mathcal{R} \), but we end this section with a reminder that this depends on a number of strong assumptions that are likely to be incorrect in detail, including:

- \( \gamma \) and \( \phi^C_{SF} \) are both independent of time;
- \( \mathcal{R} \) depends only on the final mass of a galaxy, and on time;
- Environmental quenching includes no change in stellar mass.

A1.1 Constructing the Quiescent SMF from a Quenched Fraction

We note that when the cluster and field SMFs are not identical, the QFE cannot be simply interpreted as the fraction of field galaxies that have to be quenched and added to the field quiescent population in order to reproduce the cluster quiescent population. That is,

\[
\phi^C_Q \neq A \left[ \phi^C_Q + (QFE) \phi^F_S \right],
\]

(A16)

where \( A = \sum \phi^C / \sum \phi^F \) is the mass-independent renormalization constant. Rather, from a simple rearrangement of terms in the definition of QFE,

\[
\phi^C_Q = \frac{\phi^C}{\phi^F} \left[ \phi^C_Q + (QFE) \phi^F_S \right].
\]

(A17)

Since the cluster and field total SMF do not have the same shape, the ratio outside the brackets is not independent of mass. This is why, even though QFE is a weak function of stellar mass in GOGREEN clusters, the observed \( \phi^C_Q \) cannot be reproduced by adding a fixed fraction of field SF galaxies to the field quiescent population, as demonstrated in van der Burg et al. (2020).

It is useful to consider what function \( f(M) \) would be required so that

\[
\phi^C_Q(M) = A \left[ \phi^C_Q(M) + f(M) \phi^F_S(M) \right],
\]

(A18)

given the constraints on QFE. Here and for what follows for this subsection, we reintroduce the explicit \( M \) dependence in the equations. Combining Equations 6 and A17 we solve for \( f(M) \):

\[
f(M) = \frac{\phi^C_Q(M) / A - \phi^C_{Q,F}(M)}{\phi^F_S(M)}
\]

(A19)

\[
\approx \frac{1}{A \phi^F(M)} \left[ \frac{\phi^F(M)}{\phi^F_S(M)} + QFE(M) \right] - \frac{\phi^F_{Q,F}(M)}{\phi^F_S(M)}
\]

(A20)

\[
= \xi(M)QFE(M) + \frac{\phi^F(M)}{\phi^F_S(M)} [\xi(M) - 1],
\]

(A21)

where we have defined

\[
\xi(M) = \frac{1}{A \phi^F(M)}
\]

(A22)

for convenience. Note that, if the total SMF shape is independent of environment, then \( \xi(M) = 1/A \phi^F = 1 \) and Equation A21 reduces to \( f = QFE \). Also interesting is that \( f \neq 0 \) when \( QFE = 0 \). That is, even if the quenched fraction is identical in the cluster and the field, it is still necessary to add quenched galaxies (and star forming galaxies) on top of what would be expected from the field in a mass dependent way, to account for the different total SMF shape.

A1.2 Transition galaxies

Now consider what we learn from the excess abundance of transition galaxies, \( f^T C - f^T F \). Here \( x \) can refer to PSB, BV, GV or any other transition population. The procedure is similar to that in § A1. We will assume that any SF galaxy accreted between time \( T - \tau \) and \( T \) will be observable as a transition galaxy at time \( T \), given a lifetime
of that phase, $\tau$. Therefore we have

$$\phi^C_x \approx \int_{T-\tau}^{T} \gamma \phi^F_x \tau R(t) dt + \phi^C_{x,s}$$  \hspace{1cm} \text{(A23)}$$

$$\approx \gamma \phi^F_x \int_{T-\tau}^{T} \tau R(t) dt + \phi^C_{x,s}$$  \hspace{1cm} \text{(A24)}$$

$$\approx \gamma \phi^F_x \tau R(T) + \phi^C_{x,s},$$  \hspace{1cm} \text{(A25)}$$

where in the last step we have assumed $R$ is constant over the timescale $\tau \ll T$. The additive term $\phi^C_{x,s}$ is there to account for galaxies that meet the transition definition independently of environment, just like in Equation A4. These include all galaxies classified as type $t$, whatever the (non-environmental) cause. Recall that the term $\gamma \phi^F_x T$ in the integrand of Equation A23 is just equal to $f^F_x \phi^C$: that is, it is the number of SF cluster galaxies that would be observed at time $T$ in the absence of environmental quenching. We can evaluate $\phi^C_{x,s}$ using the field,

$$\phi^C_{x,s} = \frac{\phi^C_x}{\phi^F_x},$$  \hspace{1cm} \text{(A26)}$$

where we have written the abundances relative to some reference population $\phi^F_x$ in the field. The choice of reference is not obvious here.

It may be appropriate to assume $\phi^F_x = \phi^F$, if the transition population in the field arises primarily from sources other than quenching of SF galaxies – for example rejuvenation of Q galaxies, or scatter due to both physical causes (e.g. dust) or measurement uncertainties. On the other hand, if the field population primarily reflects the quenching of SF galaxies it would be more correct to assume $\phi^F_x = \phi^F$: leaving this general for now, we obtain

$$\phi^C_x \approx \gamma \phi^F_x T \tau R(T) + \phi^C_{x,s} \frac{\phi^C_x}{\phi^F_x}.$$  \hspace{1cm} \text{(A27)}$$

Dividing both sides by $\phi^F_x$ yields:

$$\frac{\phi^C_x}{\phi^F_x} \approx \gamma \phi^F_x T \tau R(T) + f^F_x \phi^C_{x,s} \frac{\phi^C_x}{\phi^F_x}$$  \hspace{1cm} \text{(A28)}$$

or

$$\frac{\phi^C_x}{\phi^F_x} \approx \gamma \phi^F_x T \tau R(T) + f^F_x \phi^C_{x,s} \phi^F_x.$$  \hspace{1cm} \text{(A29)}$$

Using Equation A2 for $\gamma$,

$$f^F_x \approx \gamma \phi^F_x T \tau R(T) + f^F_x \phi^C_{x,s} \phi^F_x.$$  \hspace{1cm} \text{(A30)}$$

Finally, we can write an expression for $\mathcal{R}$:

$$\tau R(T) = \frac{f^F_x - f^F_x \phi^C_{x,s}}{\phi^F_x}.$$  \hspace{1cm} \text{(A31)}$$

This gives rise to Equation 5, if the reference sample is the total sample so e.g. $\phi^C_{x,s} = \phi^C/\phi^F = 1$. We use this as our baseline, and the figures in the paper are generated under that assumption. Alternatively, we might assume that the abundance of non-environmentally related transition galaxies are proportional to the fraction of star-forming galaxies in a population, so $f^C_{x,s} = f^F_x$. This has the effect of increasing the excess found in clusters, and hence the resulting $\mathcal{R}$. If this assumption is made, we refer to $\phi^C_{x,s}$ as "primordially quenched" galaxies that remains fixed in time.

**Figure A2.** Similar to Figure 13, we show the transition rate $\mathcal{R}$ for the BQ and PSB populations, but here assuming that the non-environmentally associated transition galaxy abundances are proportional to the SF population, rather than the total. This increases the resulting rates, particularly at high stellar masses. However, the change is modest and does not qualitatively affect our conclusions.

### A2 Quenching a fixed fraction of galaxies

Alternatively, we can consider a model where a fixed fraction $Q(M, t)$ of accreted galaxies is quenched. This could correspond to a case where only a fraction of galaxies are on the right orbits to be quenched - and they either are or aren’t, in a binary way. Equation A5 becomes

$$\phi^C_Q = \int_{0}^{T} \gamma \phi^F_s Q dt + \phi^C_{Q,s}$$  \hspace{1cm} \text{(A32)}$$

$$\approx \gamma \phi^F_s \int_{0}^{T} Q dt + \phi^C_{Q,s},$$  \hspace{1cm} \text{(A33)}$$

Following through with the same algebra as in § A1, we end up with

$$QFE = \frac{f^C_Q - f^F_Q}{f^F_s} \approx \frac{1}{T} \int_{0}^{T} Q(t) dt.$$  \hspace{1cm} \text{(A34)}$$

If $Q$ is constant, then $QFE = Q$. This would be perhaps the simplest way to get a QFE that is independent of redshift and stellar mass.

### A3 Primordial population

Finally, let’s consider the case where there is no accretion-based quenching at all, but the cluster simply starts with a population of "primordially quenched" galaxies that remains fixed in time.

$$\phi^C_Q = \phi^C_{Q,p} + \phi^C_{Q,s}$$  \hspace{1cm} \text{(A35)}$$

$$= \phi^C_{Q,p} + \phi^F \phi^C$$  \hspace{1cm} \text{(A36)}$$

$$= \phi^C_{Q,p} + f^F \phi^C$$  \hspace{1cm} \text{(A37)}$$

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Dividing both sides by $\phi^C$ then gives

$$f_Q^C = \frac{\phi_{Q,p}}{\phi^C} + f_F^C. \quad (A38)$$

So QFE is simply

$$QFE = \frac{f_Q^C - f_F^C}{f_S^F} = \frac{f_Q^C}{f_S^F}. \quad (A39)$$

Note that $f_{Q,p}^C$ will decrease with time, since (we assume) the primordial population $\phi_{Q,p}$ remains constant while the cluster $\phi^C$ grows around it. This can lead to a roughly constant QFE, since both $f_{Q,p}^C$ and $f_S^F$ decrease slowly with time. However, it would not be natural to expect it to be constant with $M$, since $f_{Q,p}$ presumably increases with $M$, while $f_S^F$ decreases.

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