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Investigating Recent Changes in MJO Precipitation and Circulation in Multiple Reanalyses

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Abstract

Recent work using CMIP5 models under RCP8.5 suggests that individual multimodel mean changes in precipitation and wind variability associated with the Madden-Julian oscillation (MJO) are not detectable until the end of the 21st century. However, a decrease in the ratio of MJO circulation to precipitation anomaly amplitude is detectable as early as 2021–2040, consistent with an increase in dry static stability as predicted by weak temperature gradient balance. Here, we examine MJO activity in multiple reanalyses (ERA5, MERRA-2, and ERA-20C) and find that MJO wind and precipitation anomaly amplitudes have a complicated time evolution over the record. However, a decrease in the ratio of MJO circulation to precipitation anomaly amplitude is detected over the observational period, consistent with the change in dry static stability. These results suggest that weak temperature gradient theory may be able to help explain changes in MJO activity in recent decades.

Plain Language Summary

A recent study examined future projected changes in precipitation and wind strength associated with the Madden-Julian oscillation (MJO) in a set of anthropogenically forced warming simulations. While they showed that changes in the amplitude of individual MJO-related variables are not detectable until the end of the 21st century, they also demonstrated that a decrease in the ratio of MJO wind to precipitation anomaly amplitude is detectable as early as 2021–2040. To examine whether these MJO changes found in climate models are realistic, changes to MJO variability are assessed in three observational products, and we find that a similar decrease in the ratio of MJO wind to precipitation strength is detectable over 1901–2018. The change in MJO activity is consistent with that expected under climate warming.

1. Introduction

The Madden-Julian oscillation (MJO; Madden & Julian, 1971, 1972) is the dominant mode of large-scale tropical precipitation variability on intraseasonal timescales. MJO activity impacts the occurrence of extreme weather events not only in tropics but also at higher latitudes due to its remote teleconnections (Zhang, 2013). Because of its ability to modulate weather across the globe, with clear implications for lives and property, extensive research is being conducted about the MJO, with increasing attention given to the evolution of the MJO under anthropogenic warming (Maloney et al., 2019). As global temperatures rise, MJO activity is expected to be impacted by competing effects, making the projections of the MJO difficult. For example, an increased basic state vertical moisture gradient in the lower troposphere increases the efficiency with which vertical motion moistens the atmosphere, leading to a strengthening of MJO-associated convection (Arnold et al., 2013; Holloway & Neelin, 2009). In contrast, an increased dry static stability decreases the efficiency by which diabatic heating induces vertical motion (Knutson & Manabe, 1995; Sherwood & Nishant, 2015; Sobel & Bretherton, 2000), which would tend to weaken MJO-associated convection (e.g., Chikira, 2014). Future projections from most global climate models (GCMs) suggest an increase in the amplitude of MJO precipitation under anthropogenic warming, although MJO circulation anomalies weaken, or at least increase less than precipitation (Maloney et al., 2019). Analysis of the reconstructed historical record from instrumental observations and reanalysis shows positive trends of MJO amplitude over the 20th century in surface pressure and precipitation (Oliver & Thompson, 2012) and in the late 20th century in zonal winds (Jones & Carvalho, 2006; Slingo et al., 1999). However, other studies have found no trend in boreal wintertime MJO amplitude from the 1980s to the 2000s when using an outgoing longwave radiation-related metric (Tao et al., 2015).
Recent evidence suggests that the MJO may undergo structural changes with warming and differences in intensification rate in its associated precipitation and circulation components. Such changes would be important because teleconnections generated by upper level divergence associated with MJO convection have a large impact on extratropical weather and its predictability (Ferranti et al., 1990; Zhang, 2013). Instead of examining the amplitude of the MJO with a single variable, Maloney and Xie (2013) and Wolding and Maloney (2015) suggest that in the deep tropics where the weak temperature gradient (WTG) approximation holds (Sobel & Bretherton, 2000), the amplitude ratio of vertical velocity to precipitation associated with the MJO is constrained by dry static stability. Since the temperature profile in the free tropical troposphere roughly follows a moist adiabat determined by convective adjustment in tropical convecting regions (Knutson & Manabe, 1995), the dry static stability profile may be constrained by future sea-surface temperature (SST) warming, thus providing a constraint on future MJO behavior.

A recent study found that the ratio of MJO-associated circulation to precipitation amplitude follows WTG balance in anthropogenic warming simulations (Bui & Maloney, 2019). The WTG approximation can be applied to the thermodynamic equation to produce the following approximate balance in the tropical free troposphere, where horizontal temperature gradients are small (Sobel & Bretherton, 2000),

\[
\omega \frac{\partial s}{\partial p} \approx Q_1
\]

where \( \omega \) is the vertical pressure velocity, \( s \) the dry static energy (DSE), and \( Q_1 \) the apparent heat source (Yanai et al., 1973). Note that all variables represent the large-scale area average. If it is further assumed that precipitation is proportional to \( Q_1 \) in MJO convective regions, and that the vertical structure of \( Q_1 \) is not changed (Maloney & Xie, 2013), it follows that at a given level,

\[
\Delta \left( \frac{\omega}{P} \right) \propto \Delta \left( \frac{\partial s}{\partial p} \right)^{-1}
\]

where \( P \) is the surface precipitation rate and \( \Delta \) denotes the relative change from a reference state to a new state. Bui and Maloney (2019) examined GCM simulations forced by Representative Concentration Pathway 8.5 (RCP8.5) in a subset of models participating in the Coupled Model Intercomparison Project 5 (CMIP5) that simulated realistic MJOs. While the amplitude changes of MJO precipitation and vertical velocity were individually not detectable until 2080, the ratio of MJO vertical velocity to precipitation amplitude showed detectable decreases as early as 2021–2040. Consistent with WTG balance and the proportionality of precipitation to \( Q_1 \), the ratio of MJO vertical velocity to precipitation amplitude matches the change in dry static stability in the simulations, implying that this theory could explain and predict the evolution of the MJO, even in the observational record that has exhibited warming.

Following this work, we investigate the temporal evolution of MJO-related precipitation and circulation amplitude and their ratio in two reanalyses (ERA5 and MERRA-2) to assess whether changes to the MJO can be detected in recent decades. A similar analysis is also applied on a century-long reanalysis (ERA-20C) to further support findings over the past few decades and to assess recent changes to the MJO in the context of low-frequency variability. Our purpose is to determine whether WTG balance can explain changes in MJO activity in the real world, which could help support projections of MJO under continued anthropogenic warming.

2. Data and Methodology

Two reanalysis data sets spanning 1981–2018 are employed to assess changes in MJO amplitude and the background environment in recent decades. The Modern-Era Retrospective analysis for Research and Applications version 2 (MERRA-2; Gelaro et al., 2017) and the European Centre for Medium-Range Weather Forecasts (ECMWF) reanalysis (ERA5; Hersbach et al., 2020) are the main data sets used to investigate MJO activity in recent decades. The ECMWF 20th century reanalysis (ERA-20C; Poli et al., 2016) is used to evaluate long-term changes in MJO behavior over 1901–2009. The MERRA-2, ERA5, and ERA-20C data sets have spatial (temporal) resolutions of \( 0.5^\circ \times 0.625^\circ \) (3 hours), \( 0.25^\circ \times 0.25^\circ \) (1 hour), and spectral truncation of T159 (1 hour), respectively. For the purpose of investigating large-scale dynamics, all variables are regridded to have a common horizontal spatial resolution of \( 2.5^\circ \times 2.5^\circ \). Vertical pressure velocity and precipitation are averaged into daily means, and temperature and DSE are originally obtained as monthly means. Wolding and Maloney (2015) imply that for good approximation, the slowly varying background DSE gradient is...
Figure 1. The boreal winter composite amplitudes of (a, b) MJO precipitation and (c, d) MJO $\omega_{400}$ during the early period (1981–1999) and (e–h) their difference from the late period (2000–2018), from (left column) ERA5 and (right column) MERRA-2. The black rectangle encloses the Indo-Pacific warm pool region, and the percentage values shown in the upper right corners of (e–h) are the area-averaged relative changes over the region.

Our focus is on the time evolution of the amplitudes of MJO precipitation and $\omega_{400}$ in the Indo-Pacific warm pool region (the IPWP region; 15°S to 15°N, 60°E to 180°) where the MJO is most active, as shown in the boxed region in Figure 1. Area-averaged MJO precipitation and $\omega_{400}$ amplitudes over the IPWP region are used as metrics to quantify overall MJO activity.

Composites obtained from 19-year running windows are extensively used in this study, similar to the averaging window length of 20 years used in Bui and Maloney (2019). This window length is chosen to reduce noise from decadal variations, but also to retain enough data points to show the time evolution of MJO activity.
Figure 2. Relative change in 19-year wintertime running composites of (a) MJO precipitation amplitude, (b) MJO $\omega_{400}$ amplitude, and (c) dry static stability at 400 hPa with respect to the early period. The x-axis denotes the central years of the associated time window, for example, 2000 denotes the period of 1991–2009. The y-axis denotes the relative change to the early period.

3. Results

First, we explore the spatial structure of MJO activity in the two reanalyses. The amplitude of MJO precipitation and $\omega_{400}$ maximize in the IPWP region (Figures 1a–1d) in both reanalyses during the early period. The changes in MJO precipitation and $\omega_{400}$ amplitude between the late period and the early period have rich spatial structures, which are similar between the reanalyses (Figures 1e–1h). Increases in both amplitudes occur to the south of India, at the southern edge of the Pacific warm pool, and near the Philippines. Decreases in both amplitudes occur near 5$^\circ$S over the Maritime Continent. The regions of large amplitude of the MJO do not change substantially between the early and late period, allowing us to assess the temporal change in MJO activity within the IPWP region. The area-averaged amplitude of MJO precipitation and $\omega_{400}$ in the IPWP region both show increases in the late period relative to the early period with precipitation intensifying by 5.6% in ERA5 and 7.6% in MERRA-2 and $\omega_{400}$ intensifying by 1.2% in ERA5 and 2.1% in MERRA-2. Most important for this study, MJO precipitation amplitude intensifies more than MJO $\omega_{400}$ amplitude in both reanalyses, although MJO activity in MERRA-2 is strengthened slightly more than in ERA5.

The 19-year running area-averaged MJO precipitation and $\omega_{400}$ amplitude in the IPWP region increase between the early and the late periods of the record, while the amplitudes in MERRA-2 exhibit larger changes than those in ERA5. However, both reanalyses demonstrate qualitatively similar fluctuations in between: in the early 1990s, both of the amplitudes rise quickly, followed by a plateau and then a slight decrease afterward (Figures 2a and 2b). The strengthening of the boreal wintertime MJO activity during the late 20th century is consistent with previous studies examining observed zonal wind changes at 200 and 850 hPa (Jones & Carvalho, 2006). Moreover, both reanalyses agree that throughout most of the record, MJO precipitation amplitude shows larger positive changes than MJO $\omega_{400}$ amplitude.

While we attempted to explain the fluctuating pattern in MJO precipitation and $\omega_{400}$ amplitude, we could find no obvious connections between them and interannual to decadal variability in surface air temperature. The evolution of surface air temperature in the IPWP region (Figure S2b) and its evolution relative to the whole tropics (Figure S2c) do not resemble the variability in the MJO amplitude time series, which have different trends from the early 1990s onward (Figures 2a and 2b). Commonly used Pacific SST indices that capture interannual to decadal variability also do not show similar variability to the MJO amplitude time series (cf. Figures 2a and 2b with Figure S3 SST indices).

To sum up, both MJO precipitation and $\omega_{400}$ amplitude increase from the early period to the late period in the IPWP region in both reanalyses, although the time evolution is non-monotonic and the amplitude of the change varies between the reanalyses. The time series of the amplitudes are not easily explained by tropical SST variability. However, a robust result common among different time periods and reanalyses is that the increase in MJO precipitation amplitude is always stronger than in MJO $\omega_{400}$ amplitude, consistent with what WTG balance would predict based on the increasing tropical static stability with SST warming observed in recent decades (Figure 2c; see also e.g., Sherwood & Nishant, 2015). We explore this contention more below.
Given a change in dry static stability, the theoretical change in the ratio of MJO $\omega_{400}$ to precipitation amplitude can be computed if one assumes that WTG balance holds (Equation 1) and that the vertical structure of $Q_1$ associated with the MJO is not changed (Equation 2). Previous modeling studies have shown good agreement between static stability changes and this ratio when applied to MJO-associated wind and precipitation variance (Bui & Maloney, 2018; Maloney & Xie, 2013; Wolding et al., 2016; Wolding & Maloney, 2015). As the climate system warms, tropical dry static stability increases in the troposphere because the atmospheric profile in the deep tropics roughly follows a moist adiabat set by the surface temperature in convecting regions (Knutson & Manabe, 1995). Consistently, increasing dry static stability has been observed in recent years as surface temperature has increased (Allen & Sherwood, 2008). Because surface temperature has increased since 1981 (Figure S2a), Equation 2 would argue for a greater change in MJO precipitation amplitude compared to MJO $\omega_{400}$ amplitude.

Figures 3a and 3b display the temporal evolution of the inverse of dry static stability and the ratio of MJO $\omega_{400}$ to precipitation amplitude ($MJO\omega_{400}/P$; see Equation 2) in ERA5 and MERRA-2. The gray diagonal line denotes the predicted theoretical relationship between MJO $\omega_{400}/P$ and inverse static stability assuming WTG theory holds and the vertical structure of the MJO remains unchanged. Between the late period and the early period (the two outlined endpoints), the decrease of the inverse of dry static stability is 2.8% in ERA5 and 4.0% in MERRA-2, and the decrease of MJO $\omega_{400}/P$ is 4.2% in ERA5 and 4.9% in MERRA-2. Consistent with WTG theory, MJO $\omega_{400}/P$ and the inverse of dry static stability show comparable decreases between the early period (1981–1999) and the late period (2000–2018). Agreement is also good in ERA5 for interim periods, especially until about 2000 (Figure 3a). Considering the complicated temporal evolution of MJO precipitation and $\omega_{400}$ amplitude (Figure 2), WTG balance provides a reasonable explanation for the evolution of MJO $\omega_{400}/P$ over the past 38 years, especially when considering the start and end of the record.

As many MJO studies use zonal wind amplitude as a metric of MJO activity (e.g., Jones & Carvalho, 2006; Slingo et al., 1999), we also examine the amplitude of MJO 850-hPa zonal wind ($u_{850}$) for reference. The evolution of the ratio of MJO circulation to precipitation amplitude is defined here using $u_{850}$ ($MJO\omega_{400}/P$). Although using $u_{850}$ is not a direct application of WTG balance in Equation 2, the amplitude of horizontal velocity should scale with vertical velocity through divergence if the vertical structure doesn’t change (Maloney & Xie, 2013). Under such conditions, we would expect a qualitatively similar decrease in the ratio of MJO $u_{850}$ to precipitation amplitude. Figure S4 shows that $u_{850}$ amplitude relative to precipitation does decrease in a qualitatively similar way, although with stronger decreases relative to $P$ than for $\omega_{400}$.

Although MJO $\omega_{400}/P$ generally follows the change in the inverse of dry static stability, there exist deviations from theoretical predictions, with maximum differences of about 1.5% in ERA5 and 4% in MERRA-2. To place these values in a larger-scale context, we compare Figures 3a and 3b to Figure 3c that shows
results from ERA-20C spanning 1901–2009. The theoretical estimate works well in ERA-20C over the whole century, with about 7–8% decreases in both MJO $\omega_{400}/P$ and inverse static stability over the century. The maximum deviation of MJO $\omega_{400}/P$ change in ERA-20C is about 2% from theoretical values predicted by the inverse of dry static stability. Deviations of ERA5 from theoretical values are even smaller than this, while deviations in MERRA-2 are larger. As described below, deviations of MERRA-2 from the theoretical estimate may occur due to the imperfect assumption of proportionality of $Q_1$ at 400 hPa and $P$.

In MERRA-2, Equation 2 overestimates the decrease in MJO $\omega_{400}/P$ in the intervening periods but works well for the two endpoints. MJO $\omega_{400}/P$ in MERRA-2 shows stronger decreases than ERA5 during the interim period largely because it has a larger $P$ amplitude change than ERA5. The exact reasons for differences between the two analyses are unclear, although they may depend on the different behavior of tropical convection simulated by the two reanalysis models. The differing DSE profile changes between ERA5 and MERRA-2 for the IPWP region (Figure S5) not only indicate differing static stability changes but also circumstantially suggest different changes to the convective heating structure between data sets given the regulation of tropical tropospheric temperature by convective heating. Such structure changes would affect how well the balance in Equation 2 reflects Equation 1, considering the assumption about the proportionality of $P$ to $Q_1$ at 400 hPa. MERRA-2 exhibits more warming in the lower troposphere than ERA5, presumably associated with increased condensational heating and precipitation generation there, which would produce greater decreases in MJO $\omega_{400}/P$ than that expected by looking at the 400 hPa level in isolation. The rate of increase in low-level warming in MERRA-2 is particularly strong until the 19-year period centered on 1997, possibly consistent with the greater MJO precipitation amplitude increase in MERRA-2 during that time than ERA5 (Figure 2), although translating mean state convective structure changes to those on subseasonal timescales should be done with care.

An examination of MJO anomaly amplitudes of $Q_1$ at 400 hPa and precipitation suggests a weaker consistency between the two quantities in MERRA-2 (Figure S6), consistent with possible vertical structure changes. However, while the change in the ratio of $\omega_{400}$ to $Q_1$ amplitude at 400 hPa generally follows dry static stability in ERA5, the agreement is not as good as in MERRA-2 (Figure S7), which might also explain some of the differing behavior in Figure 3. The reasons for this discrepancy are unclear.

### 4. Summary

The changes to MJO precipitation and $\omega_{400}$ amplitude from 1981 to 2018 are examined in three reanalysis data sets: ERA5, MERRA-2, and ERA-20C. Both amplitudes in ERA5 and MERRA-2 individually increased from the early period (1981–1999) to the late period (2000–2018) (Figure 1). However, their temporal behavior is non-monotonic in that both amplitudes intensify from 1981 to 1997 and slowly weaken or remain constant thereafter (Figures 2a and 2b). Interannual-to-decadal surface temperature variability (Figures S2 and S3) shows no simple relationship with this non-monotonic behavior in MJO activity changes.

When viewed together, amplitude changes of MJO precipitation are larger than MJO $\omega_{400}$ throughout the past four decades relative to the early period (1981–1999). A preferential strengthening of MJO precipitation amplitude relative to MJO $\omega_{400}$ amplitude is predicted by WTG balance with a warming climate, in that increasing dry static stability in response to SST warming in recent decades makes vertical motion more efficient at compensating latent heat release in deep convective regions. The fractional amplitude changes in the ratio of MJO $\omega_{400}$ to precipitation between 1981–1999 and 2000–2018 approximately match inverse dry static stability changes with climate warming, consistent with WTG balance (Figures 3a and 3b). A similar result is shown in ERA-20C between 1901–1919 and 1991–2009 (Figure 3c).

While trends in these reanalyses appear to generally follow WTG balance, differences exist in the behavior of the three reanalyses. MJO precipitation and $\omega_{400}$ amplitude increases are larger in MERRA-2 than in ERA5, especially in intermediate periods between the beginning and end of the record, although they show qualitatively similar time series variability (Figure 2). Decreases in MJO $\omega_{400}/P$ also fit the theoretical prediction based on the inverse of dry static stability better in ERA5 and ERA-20C than in MERRA-2 across all 19-year periods examined in terms of RMSE, and these differences may be associated with differences in the simulated structure of tropical deep convection, which remains a topic for further investigation.

The present paper provides a preliminary assessment of MJO activity changes in precipitation and vertical velocity over the past four decades that include both anthropogenic forcing and natural variability and uses a
century-long data set to assess recent changes in the context of natural variability over the longer record. Our results based on observations support those previously derived from climate models (e.g., Bui & Maloney, 2019) suggesting that decreases in MJO $\omega_{os}/P$ occur as surface temperatures warm due to anthropogenic forcing. Nevertheless, discrepancies between results from ERAs and MERRA-2 leave lingering questions about the degree to which changes to the MJO can be explained by WTG theory, including the assumption that $Q_s$ has no vertical structural changes in response to climate warming. Further work using a broader set of observational data including tropical sounding and other in situ records is needed to affirm the validity of Equation 2 for explaining MJO behavior.

Data Availability Statement
Data can be accessed online (ERAs: https://cds.climate.copernicus.eu; MERRA-2: https://gmao.gsfc.nasa.gov/reasanalysis/MERRA-2/data_access; ERA-20C: https://www.ecmwf.int/en/forecasts/datasets/reasanalysis-datasets/era-20c; OMI: https://www.psl.noaa.gov/mjo/mjoindex; Niño 3.4: https://climatedataguide.ucar.edu/climate-data/nino-sst-indices-nino-12-3-34-4-oni-and-tni; PDO index: https://www.ncdc.noaa.gov/teleconnections/pdo; and TPI: https://psl.noaa.gov/data/timeseries/IPOTPI).

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