On Repetition Protocols and Power Control for Multiple Access Block-Fading Channels

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Abstract—In this paper we study the long-term throughput performance of repetition protocols coupled with power control for multiple access block-fading channels. We propose to use the feedback bits to inform the transmitter about the decoding status and the instantaneous channel quality. We determine the throughput of simple and practically inspired protocols; we show remarkable throughput improvements, especially at low and moderate SNR, when compared to protocols where the feedback bits are used for acknowledgment only or for power control only; we show that the throughput is very close to the ultimate ergodic multi-user water-filling capacity for small number of feedback bits and/or retransmissions. For symmetric Rayleigh fading channels, numerical results show that the throughput improvement is mainly due to the ability to perform a power control, rather than to retransmit.

I. INTRODUCTION

In current networks, reliability is obtained with a combination of FEC (Forward Error Correction) and HARQ (Hybrid Automatic Repetition reQuest). FEC attempts to correct transmission errors by using error correcting codes (convolutional codes, turbo codes, etc.), while HARQ protocols request a retransmission when an error is detected. HARQ protocols require a feedback channel to indicate a decoding success/failure to the transmitter. In wireless channels without CSI (Channel State Information), HARQ provides time diversity and robustness to channel variations [1]. If CSI is available at the transmitter, adaptive rate and power allocation becomes possible [1]. Although power control improves the performance of single-user channels at low SNR (Signal to Noise Ratio) only, it is well known to provide multi-user diversity in MAC’s (Multiple Access Channel) [2]. The central question of this paper is: with the objective to maximize the network throughput, should the available feedback resources be used for HARQ, or to provide CSI? In this paper, we consider fading MAC’s. We propose that the available feedback bits are used to communicate to the transmitter both the decoder state and the channel state, as proposed in [3] for single-user channels. Our goal is to simultaneously realize the gains of power control and of repetition protocols by using the same feedback resources that would be used for repetition alone.

We assume that the CSI (i.e., the fading gains from the transmitters to the receiver) is perfectly known at the receiver, for example through pilot tones. The receiver then informs the transmitters about the channel and the decoder state through a common (broadcast) feedback channel of finite capacity. Since the feedback channel is rate-limited, the transmitters only have partial CSI, based on which they need to decide an appropriate power level for the (re)transmission. Past work considering limited CSI only focused on ergodic capacity or on outage probability, but not on HARQ protocols—which is the goal of this paper. For example, the work in [4] showed that power control is very useful to minimize the outage probability even with partial and/or noisy CSI, while the work in [5] derived the ergodic capacity of the MAC with perfect CSI.

Here we extend the joint HARQ and power control protocol proposed in [3] for a single-user channel to MACs. The protocol in [3] is equivalent to a time-varying (depending on the current retransmission attempt) quantizer of the amount of redundancy that is still needed at the decoder for successful decoding. The novel technique of [3] improves the long-term average throughput at any SNR, compared to schemes with power control and/or HARQ alone; moreover, it achieves at least 67% of the ergodic water-filling capacity with a single retransmission and one bit of feedback. The ergodic water-filling capacity is the fundamental performance limit of a fading channel with perfect CSI and with the possibility to code across many channel coherence times, i.e., it is achievable when a feedback channel of infinite capacity is available (to provide perfect CSI to the transmitter) and there is no upper limit to the number of retransmissions (to ensure zero outage).

In this paper, we consider a $K$-user block-fading Gaussian MAC where each user has $M$ transmission attempts to send a data packet to the central receiver. The receiver is assumed to have an error-free broadcast feedback channel of capacity of $\log_2(F)$ bits to communicate to the transmitters. Our performance measure includes the outage capacity [8] and the ergodic capacity [2] as a special case for $M=1$ and $M=\infty$, respectively [9]. For a finite $(M,F)$, deriving the optimal throughput, or an outer bound, seems very difficult. For this reason, we propose some simple and practically inspired schemes, we evaluate their throughput, and compare them with the ultimate ergodic water-filling capacity (i.e., case $(M,F) = (\infty, \infty)$).

The rest of the paper is organized as follows: Section [II] introduces the system model; Section [III] proposes various policies for $M=1$; Section [IV] discusses the case of $M \geq 2$; Section [V] reports numerical results, and Section [VI] concludes the paper.
II. SYSTEM MODEL

Notation: \( \mathbb{E}[X] \) is the expected value and \( F_X(x) \) is the cumulative distribution function (cdf) of the random variable \( X \). \( P[A] \) is the probability of the event \( A \). \( N \), \( R \) and \( C \) indicate, respectively, the natural, the real and the complex numbers.

Plots show the ratio of throughput (finite \((M, F)\)) and ergodic capacity (\((M, F) = (+\infty, +\infty)\)) vs SNR in dB. The numerical results are for unit power Rayleigh fading, i.e., the fading power has \( cdf F_X(x) = 1 - e^{-\max(x,0)^+} \), for which the
\[
\mathbb{E}[1/X \cdot 1_{\{X>x\}}] = \text{Ei}(x) = \int_x^{\infty} e^{-t/t} \, dt, \ x \geq 0.
\]
Equations labeled with \( \ast \) hold for for a symmetric system where all users have the same power constraint, the same transmit rate, and the same fading iid Rayleigh fading; in this case we shall drop the index of the user.

Modeling Assumptions: We consider a block-fading Gaussian MAC. The receiver knows perfectly the channel fading at the beginning of each slot, whereas the transmitters have no CSI, unless explicitly informed by the receiver. Transmitters can not modify the rate of communication in each slot and cannot send a superposition of different codebooks, as opposed to [10] and to [11] which considered multi-layer transmission. Power allocation is instead permitted, exploiting the partial CSI obtained from the receiver. Each transmitted codeword spans one fading block, or slot, over which the fading is constant. The slot length is sufficient to permit successful decoding if the mutual information at the receiver is above the transmission rate [8]. The broadcast feedback channel is assumed error-free, delay-free and of finite capacity given the transmission rate [8]. The broadcast feedback channel is assumed error-free, delay-free and of finite capacity given by \( \log_2(F), \ F \in N. \) Accumulation of feedback bits over successive slots is not permitted. The receiver can detect uncorrectable errors and in this case can ask for a retransmission. Each transmitter can transmit at most \( M \) times, \( M \in N, \) the same data packet, including the first transmission. The performance measure is the long-term average throughput vs. the long-term average power. Long-term means that that the averages are evaluated over a time horizon much larger than \( M. \) Power control permits to use more power when the instantaneous channel conditions are “good”, as long as the average power constraint is not violated. Peak power constraints, although important in practice, are not considered in this paper and are left for future work.

Performance Measure: Under these assumptions, the received signal in slot \( t \in N \) of a \( K \)-user MAC is:
\[
Y_t = \sum_{k=1}^{K} h_{k,t} \sqrt{P_{k,t}} X_{k,t} + Z_t \in C^{n \times 1} \tag{1}
\]
where: \( h_{k,t} \) is the fading gain for user \( k, \) \( Z_t \) is the AWGN with zero mean and unit variance, \( X_{k,t} \) is the Gaussian codeword of length \( n, \) such that \( 1/n \mathbb{E}[|X_{k,t}|^2] = 1, \) and \( P_{k,t} \) is the instantaneous power that must satisfy the power constraint \( P_k, \) that is, \( \lim_{T \to \infty} 1/T \sum_{t=1}^{T} P_{k,t} \leq P_k. \) We assume \( P_{k,t} \in \{ P_k^{(1)}, \ldots, P_k^{(M)} \} \), where \( P_k^{(m)} \) is the power policy to be used at the \( m \)-th transmission attempt, \( m = 1, \ldots, M, \) that can take at most \( F \) values.

Let \( R_{k,t} \) be the rate decoded at time \( t \) for user \( k. \) The throughput is
\[
\eta_{M,F,K} = \lim_{T \to \infty} 1/T \sum_{t=1}^{T} (R_{1,t} + \cdots + R_{K,t}).
\]
For any \((M, F),\) the throughput is upper bounded by the ergodic water-filling capacity (ewfc)
\[
\eta_{M,F,K} \leq \eta_{K}^{(ewfc)} = \sum_{k=1}^{K} (-1)^{k-1} \left( \begin{array}{c} K \\ k \end{array} \right) \text{Ei}(kx), \tag{2}
\]
where \( x \geq 0 \) is linked to the power constraint through
\[
P_k \leq \sum_{k=1}^{K} (-1)^{k-1} \left( \begin{array}{c} K \\ k \end{array} \right) (e^{-kx} - kx \text{Ei}(kx)). \tag{3}
\]

III. CASE \( M = 1: \) OUTAGE CAPACITY

In the following we introduce protocols/policies for the case where only one transmission per data packet is allowed (i.e. \( M = 1. \) Policies are divided into two categories: a) those that do not exploit CSI and, therefore, are not able to perform power adaptation, and b) TDMA-type policies, where the user with the largest fading gain is allowed to transmit at any give time (thus requiring CSI). Although the proposed policies are not throughput optimal, we will show that they achieve a large fraction of the ergodic water-filling capacity \( \eta_{K}^{(ewfc)} \) in (2).

Policies without CSI (i.e. \( F = 1): \) Let parametrize the rates as \( R_u = \log(1 + s_u P_u) \) for some \( s_u \geq 0, \ u = 1, \ldots, K, \) to be optimized. Consider a static TDMA scheme, where each user sends for a fraction \( 1/K \) of the time with power \( P_u = K P_u. \) The throughput is
\[
\eta_{M=1,F=1,K}^{(static-TDMA)} = \max_{s_1, \ldots, s_K} \sum_{k=1}^{K} 1/K \log(1 + s_k K \mathbb{P}[|h_k| > s_k])
\]
\[
= \max_{s \geq 0} \left\{ e^{-s} \log(1 + s K \mathbb{P}) \right\} = \eta_{single}(K \mathbb{P}). \tag{4}
\]
If the transmitters are allowed to transmit simultaneously, then the receiver must perform joint decoding. For the case of \( K = 2 \) users (extensions to more than two users is straightforward) we get
\[
\eta_{M=1,F=1,K=2}^{(joint)} = \max_{R_1, R_2} \left\{ R_1 \cdot P_{10} + R_2 \cdot P_{01} + (R_1 + R_2) \cdot P_{11} \right\}
\]
\[
= \max_{s \geq 0} \left\{ 2 e^{-s} \left( \frac{1 - e^{-s(P_s + 1)}}{P_s + 1} + e^{-s(P_s + 1)}(P_{s+1}) \right) \right\} \cdot \log(1 + P_s) = \eta_{joint}(P), \tag{5}
\]
where
\[
P_{11} = \mathbb{P} R_1 \leq \log(1 + |h_{1,t}|^2 P_{1,t})
\]
\[
P_{10} = \mathbb{P} R_1 \leq \log(1 + |h_{2,t}|^2 P_{2,t})
\]
\[
P_{20} = \mathbb{P} R_2 \leq \log(1 + |h_{1,t}|^2 P_{1,t})
\]
\[
P_{21} = \mathbb{P} R_2 \leq \log(1 + |h_{2,t}|^2 P_{2,t})
\]
\[
\text{is the probability that the two users can be jointly decoded,}
\]
\[
P_{10} = \mathbb{P} R_1 \leq \log\left(1 + \frac{|h_{1,t}|^2 P_{1,t}}{1 + |h_{2,t}|^2 P_{2,t}}\right)
\]
\[
P_{20} = \mathbb{P} R_2 \leq \log\left(1 + \frac{|h_{2,t}|^2 P_{2,t}}{1 + |h_{1,t}|^2 P_{1,t}}\right)
\]
\[
\text{is the probability that user 1 can be decoded by treating user 2 as noise and that user 2 cannot be decoded, and } P_{01} \text{ is as } P_{10}
\]
\[
\text{but with the role of the users swapped. In the case } M =
\]
In the symmetric case it can be shown that $\lambda_u = \tau_u = s$ for all $u = 1, ..., K$ is optimal and that

$$
\eta^{(cdTDMA-on/off)}_{M=1,F=K+1,K} = \max_{s \geq 0} \left( 1 + \frac{sK}{1 - (1 - e^{-s})^K} \right) \left[ 1 - (1 - e^{-s})^K \right],
$$

(8)

It is immediate to see $\eta^{(cdTDMA-on)}_{M=1,F=K,K} \leq \eta^{(cdTDMA-on/off)}_{M=1,F=K,K}$.

We could also consider "hybrid" policies where joint decoding and cdTDMA coexist (joint+cdTDMA). In [12], we analyzed such more complex power policies for $M = 1$; it turned out that the improvement over cdTDMA-on/off is minimal and does not justify the increased in complexity.

The policies discussed so far used are characterized by $\log_2(F) \leq K$, that is, the amount of feedback resources per user is the same as that of a simple HARQ protocol. We next show how to get closer to the ergodic water-filling capacity by allowing $\log_2(F) > K$. We shall see that the ability to perform a finer channel adaptation (due to a better CSI) greatly increase the achievable throughput. The previous cdTDMA-on/off policy allowed for the instantaneous power to be either zero or $P_\lambda > 0$ and required $F = K + 1$ feedback values. We extend it now so that the instantaneous power can be from the set $\{0, P_1, ..., P_L\}$ with $0 < P_1 < ... < P_L$ thus requiring $F = LK + 1$ feedback values. We refer to this policy as multilevel cdTDMA-on/off. We only discuss the symmetric systems; the extension to a general setting is straightforward. Let $s_0 = 0 < s_1 < ... < s_L < s_{L+1} = \infty$ be free parameters to be optimized and parameterize the powers as $P_\ell = (e^{R - 1})/s_\ell$, $\ell = 1, ..., L$. User $u$ can transmit with power $P_\ell$ if $B = \ell + K(u - 1)$, where $u$ and $\ell$ are chosen to satisfy

$$
u = \arg \max_{k=1,...,K} \{b_k^2\}$$

and zero otherwise. With this choice of feedback and power levels, successful decoding is always possible except when $B = 0$, thus the throughput is

$$
\eta^{(multilevelcdTDMA-on/off)}_{M=1,F=1+KL,K} = \max_{\{s_\ell\}} \left( 1 + \frac{\sum_{\ell=1}^{L} \frac{P_\ell}{s_\ell}}{F} \right) (1 - (1 - e^{-s_\ell})^K),
$$

(9)

with

$$
P[F = \ell] = \Pr[s_\ell < \min_{u=1,...,K} \{b_u^2\} \leq s_{\ell+1}].$$

When $L \to \infty$, the multilevel cdTDMA-on/off scheme reduces to "truncated channel inversion" [6], which is the optimal in the sense of minimizing the outage probability for a long-term power constraint.

IV. CASE $M \geq 2$ ($M - 1$ POSSIBLE RETранSMISSIONS)

In the previous section (see [9]) we saw that the throughput increases with $F$. In this section we evaluate the throughput improvement due to an increase in the number of retransmissions $M$. We focus on chTDMA-type policies only, as they
emulate the power allocation that achieves the ergodic water-filling capacity. We shall only consider protocols for symmetric scenarios; extension to general scenarios is straightforward but tedious.

cdTDMA+ALO: Here we consider in detail the case \( K = M = 2 \), but the analysis extends easily. We start by considering a scheme where a user is scheduled to transmit when it has the largest fading gain among all users, and its fading is large enough to grant successful decoding for the available transmit power; in this case an outage occurs if a user is not scheduled for transmission for \( M \) consecutive time slots; the scheme requires \( F = 1 + K \) feedback values.

As shown in [3], by knowing the average reward/decoded rate \( \mathbb{E}[R] \), the average cost/transmit power \( \mathbb{E}[\mathcal{T}] \), and average inter-renewal time/decoding time \( \mathbb{E}[\mathcal{T}] \), the long-term average throughput is \( \mathbb{E}[\mathcal{R}]/\mathbb{E}[\mathcal{T}] \) and the long-term average power is \( \mathbb{E}[\mathcal{P}]/\mathbb{E}[\mathcal{T}] \). The computation of these quantities if not straightforward in a multiuser channel. Imagine the protocol as a finite state machine with states: \((1, 1)\): both users are at the first transmission attempt; \((1, 2)\): user 1 is at the first transmission attempt, while user 2 is at the second (and last); \((2, 1)\): user 1 is at the second transmission attempt, while user 2 is at the first; \((2, 2)\): both users are at the second transmission attempt and can not retransmit the same packet any more. A renewal occurs when the system is in the state \((1, 1)\). A state diagram describing the possible transitions among states is given in Fig. 1 where the possible feedback values over two consecutive slots that grant the corresponding transition are indicated over each arrow. Given the usual parameterization of rates and powers with the threshold \( s > 0 \), we can define the probabilities of each feedback value: \( \mathbb{P}[B = 0] = \mathbb{P}[\max(|h_1|^2, |h_2|^2) \leq s] = (1 - e^{-s})^2 = 1 - p \), and by symmetry \( \mathbb{P}[B = 1] = \mathbb{P}[B = 2] = p/2 \).

From the state diagram in Fig. 1 we can compute the stationary distribution of the corresponding aperiodic and irreducible Markov chain, which we denote by \( \pi; \pi_{i,j} = \mathbb{P}[\text{state } (i, j)] \). With simple algebra, one finds that the average inter-renewal time is

\[
\mathbb{E}[\mathcal{T}] = \frac{1}{\pi_{1,1}} = 4 - p. \tag{10}
\]

In order to evaluate the average reward, we must understand the evolution of the protocol with time, which is depicted in Fig. 2. In Fig. 2 the state \((1, 1)\) correspond to renewal events, i.e., the systems starts anew. Let isolate the right branches starting from the state \((2, 2)\) at time \( \tau = 1 \) and compute the accumulated reward. Only the branches labeled with \( p/2 \) contribute to the reward as they correspond to successful decoding of rate \( \mathcal{R} \), that is, \( \mathbb{E}[\mathcal{R}]_{|\mathcal{R}=\mathcal{R} > 0} = R p (1 - p) \). For the left branches, the accumulated reward as a function of the time \( \tau \) can be expressed by using the Pascal’s triangle as follows:

\[
\sum_{k=0}^{\tau-2} 2 R \binom{\tau - 2}{k} \left( \frac{p}{2} \right)^{k+2} (1 - p)^{\tau-2-k} = \left( \frac{p}{2} + (1 - p) \right)^{\tau-2} + (\tau - 2) \left( \frac{p}{2} + 1 - p \right)^{\tau-3} \left( \frac{p}{2} \right). \tag{11}
\]

The average reward, not considering the left branches is thus

\[
\mathbb{E}[\mathcal{R}] = 2 R \left( \frac{p}{2} \right)^2 \sum_{\tau=2}^{\infty} 2 \left( 1 - \frac{p}{2} \right)^{\tau-2} + \sum_{\tau=2}^{\infty} (\tau - 2) \left( 1 - \frac{p}{2} \right)^{\tau-3} \left( \frac{p}{2} \right] = 3 p R. \tag{11}
\]

By summing the two average reward terms, we get

\[
\mathbb{E}[\mathcal{R}] = \mathbb{E}[\mathcal{R}]_{|\mathcal{R}=\mathcal{R} > 0} + \mathbb{E}[\mathcal{R}]_{|\mathcal{R}=\mathcal{R} > 0} = R p (4 - p). \tag{11}
\]

and thus

\[
\eta^{(\text{cdTDMA+ALO})}_{M=2, F=3, K=2} = \max_{R > 0} \frac{\mathbb{E}[\mathcal{R}]}{\mathbb{E}[\mathcal{T}]} = \max_{R > 0} R p. \tag{12}
\]

We recognize that the throughput in (12), with \( R = \log(1 + 2s/p) \), is the same as the case \( M = 1 \) in [3]; therefore a retransmission in this case does not improve performance. Intuitively, this is so because this protocol is equivalent to the Aloha (ALO) scheme in [9] (because only one transmission is taken into account for decoding).

cdTDMA+INR: Here we propose to extend the previous cdTDMA+ALO scheme so as to include \( L > 1 \) non-zero transmit power levels; in this case each user adopts the single-user HARQ protocol with Incremental Redundancy (INR) of [3] when scheduled to transmit; the scheme requires \( F = 1 + L K \) feedback values. Let \( \eta^{(\text{INR})}_{M, F, K=1} (\mathcal{P}^L; F_{H^2}) \) be the throughput of the single-user INR protocol in [3] pp.1299] with power constraint \( \mathcal{P}^L \) over a fading channel with fading power gain distributed as \( F_{H^2} \). The throughput of the cdTDMA+INR protocol is

\[
\eta^{(\text{cdTDMA+INR})}_{M, F=1 + K L, K = 1} = \eta^{(\text{INR})}_{M, F=1 + K L, K = 1} (K \mathcal{P}^L; F_{\max(|H_1|^2, . . . , |H_K|^2)}), \tag{13}
\]
because, in a symmetric network, a user is active for a fraction $1/K$ of the time when is fading gain is distributed as $F_{\max}\{|H_1|^2,\ldots,|H_K|^2\}$.

V. NUMERICAL RESULTS

In this section we numerically evaluate the throughput of the different protocols introduced in this paper for a symmetric iid Rayleigh fading two-user MAC. Although we did not attempt to optimize the throughput for a finite $(M,F)$-pair, we now show that small values of $F$ and/or $M$ get close to the water-filling ergodic capacity (case $(M,F) = (+\infty, +\infty)$). Fig. 3 shows the normalized achievable throughput of the various protocols; the normalization is with respect to the ergodic water-filling capacity $\eta_{K}^{(\text{water})}$.

Case $M = 1$ and $F = 1$: From Fig. 3 the static TDMA protocol with joint decoding $\eta_{M=1,F=1,K=2}^{(\text{joint})}$ in (3) has the worst performance at very low SNR. The static TDMA protocol with no concurrent transmissions $\eta_{M=1,F=1,K=2}^{(\text{static-TDMA})}$ is better than $\eta_{M=1,F=1,K=2}^{(\text{joint})}$ at very low SNR because only one user is allowed to transmit at any give time, which makes the system interference-free. At high SNR instead, joint decoding of $\eta_{M=1,F=1,K=2}^{(\text{joint})}$ increases the throughput over $\eta_{M=1,F=1,K=2}^{(\text{static-TDMA})}$. The protocol $\eta_{M=1,F=1,K=2}^{(\text{joint+TDMA})}$ in (6) combines the advantages of $\eta_{M=1,F=1,K=2}^{(\text{joint})}$ and $\eta_{M=1,F=1,K=2}^{(\text{static-TDMA})}$ and outperforms both. This shows that joint decoding does not substantially improve throughput.

Case $M = 1$ and $F \geq 2$: The slight performance enhancement of $\eta_{M=1,F=2,K=2}^{(\text{cdTDMA---on})}$ in (7) with respect $\eta_{M=1,F=1,K=2}$ is due to the fact that the best user is always selected for transmission thus reducing the probability of decoding failure. This shows that scheduling alone (without power control) is not sufficient to significantly boost performance. A performance increase is obtained with $\eta_{M=1,F=3,K=2}^{(\text{cdTDMA---on/off})}$ in (9) with respect to $\eta_{M=1,F=1,K=2}$, especially at low SNR. This is because CSI allows to turn off power when the channel is in a deep fade; this policy achieves no less than 67% of the ergodic water-filling capacity with just $1/2 \log_2(3) = 0.8 < 1$ feedback bits per user. Similar observations hold for $\eta_{M=1,F=7,K=2}^{(\text{multilevel cdTDMA---on/off})}$ in (9) this policy achieves no less than 81% of the water-filling ergodic capacity with just $1/2 \log_2(7) = 1.4$ feedback bits per user. This shows that power control, even based on coarsely quantized CSI, is the best way to improve performance, especially at low SNR.

Case $M = 2$ and $F \geq 2$: The highest throughput is obtained with $\eta_{M=2,F=7,K=2}^{(\text{cdTDMA+INR})}$ in (13), here evaluated for $F = 7$ so as to compare the benefits of one retransmission with $(\text{multilevel cdTDMA---on/off})^2$; this policy achieves no less than 85% of the water-filling ergodic capacity with less than two bits of feedback per user and one retransmission. Although we only evaluated the throughput for a two-user MAC, we predict even larger gains from an increase in number of users $K$ because the protocol $\eta_{M,F=1+K,L,K}^{(\text{cdTDMA+INR})}$ is able to combine the advantages of power control with those of multi-user diversity.

VI. CONCLUSIONS

We consider the problem of how to best use the limited feedback resources in block-fading MACs: to provide CSI (to gain multi-user diversity), or to enable HARQ (to gain time diversity)? We considered the long-term average throughput as a figure of merit and we showed that power control (i.e., CSI at the transmitter) seems to be a key factor to improve the throughput in a two-user iid Rayleigh fading MAC with about one bit of feedback per user. We are currently working on extending the result of this work to systems with larger number of users $K$, larger number of retransmissions $M$, larger number of feedback bits $\log_2(F)$, and different fading statistics to assess the generality of our result.

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