Research Article

Experiment, Optimization, and Design of Electromagnetic Track Brake for High-Speed Railways System

Chun Xiang,1 Jun-Cheng Wang,2 Yu-Feng Gu,2 Shi-Jin Zhang,2 and Shi-An Chen1,2

1College of Mechanical and Automotive Engineering, Zhejiang University of Water Resources and Electric Power, Hangzhou, China
2School of Automobile and Traffic Engineering, Jiangsu University, Zhenjiang, China

Correspondence should be addressed to Shi-An Chen; chensa@zjweu.edu.cn

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To enhance braking force and control convenience of high-speed railway systems, this paper proposes a new electromagnetic track brake, and the corresponding design, optimization, and experimental test are implemented. The proposed track brake is longitudinal-axis magnetic circuits excited by multiple coils electromagnets, and the pole shoes are extending outward. A preliminary design of an electromagnetic track brake is developed, including iron core height, iron core width, iron core gap, excitation ampere-turn, coil arrangement form, coil thickness, and preliminary height of single-layer coil. The electromagnet number and pole shoe gap are optimized through three-dimensional electromagnetic simulation comparisons. The final design of the electromagnetic track brake is determined, including iron core length, copper wire diameter, coil turn, and final height of single-layer coil. Experimental verification of electromagnetic attractive force is performed through prototype tests, and the newly developed electromagnetic track brake can enhance electromagnetic braking deceleration by 39%.

1. Introduction

Since the high-speed rail system Shinkansen was first launched in 1964, such rail systems have developed rapidly in Japan, Germany, France, and China [1, 2]. The current maximum speed of high-speed trains reportedly reached 574.8 km/h [3]. Reducing speed of trains as quickly as possible during emergencies is important. Magnet track brake is employed together with the main wheel-rail brake system in emergency circumstances because it is independent of wheel-rail adhesion [2, 4]. Moreover, magnet track brake was reported to be used against slippery tracks caused by contaminants such as snow, sand, and leaves, among others [5].

During operation of magnet track brake, its brake shoes are driven by magnets to attract and contact track. A sliding motion occurs between pole shoes and track to generate braking force (BF) [6]. Magnet track brakes can be categorized into permanent-magnet track brake and electromagnetic track brake (ETB), classified by the excitation mode [7]. Magnet circuit of ETB has two layout forms, namely, lateral-axis form and longitudinal-axis form [8].

To enlarge braking force and control convenience of high-speed railway systems, this research presents a new ETB. The proposed ETB has two outstanding characteristics. The first characteristic is its use of a longitudinal-axis magnetic circuit excited by electromagnets with multiple coils in parallel. This coil arrangement can achieve step control on BF to achieve good control convenience when the exciting voltage is fixed. The second characteristic is pole shoes extending out. The extended pole shoes can enlarge the contact area between pole shoes and track to enhance BF. Furthermore, the enlarged contact area can increase brake service life. Safety is the most important factor when an emergency occurs. Therefore, a battery is chosen as an excited power source to ensure working reliability of ETB. As the battery voltage in high-speed railway carriages in China (CRH) is 24 V [3], a new ETB design, its optimization, and experimental verification are necessary.

The measures of iron core, coil, protection block, and longitudinal beam are ascertained in this research. Iron core gap, coil arrangement form, and excitation ampere-turn are also determined. Electromagnet number and pole shoe gap
are optimized through simulations to attain the largest electromagnetic attractive force (EAF) [5, 6]. Finally, an experimental verification of an EAF between the proposed ETB and track is conducted through prototype tests.

The contributions of this study are summarized as follows: (1) a new ETB excited by a battery with longitudinal-axis magnetic circuits and extended pole shoes is proposed; (2) the electromagnet number is optimized to be six, and the pole shoe gap is optimized to be 40 mm, which significantly improve BF; (3) the proposed ETB can enhance braking deceleration by 39% unlike the one for ICE, thereby improving braking security significantly; and (4) the availability of ETB is experimentally verified, which provides reference for ETB design.

This paper is organized as follows: first, a preliminary design of ETB is developed, including iron core height, iron core width, iron core gap, excitation ampere-turn, coil arrangement form, coil thickness, and the height of the single-layer coil. Then, simulations are carried out, and optimization results are presented. Second, the final design of the ETB based on the optimization is created, including iron core length, copper wire diameter, coil turns, and the final height of the single-layer coil. Third, the experimental verification of EAF is conducted. Finally, the BF is calculated.

## 2. Preliminary Design of ETB

The iron core and pole shoe widths are decided according to track width. The numerical range of the iron core length is calculated through magnetic circuit analysis. The excitation ampere-turn is obtained according to magnetic circuit analysis, and equivalent air gap between pole shoes and track belong to the preliminary design. The coil arrangement form, winding thickness, coil height, iron core height, pole shoe height, the measures of protection block and longitudinal beam, adjacent iron cores gap, and the gap between protection block and adjacent iron core are determined in this part.

The material of the longitudinal beam, iron core, pole shoe, and protection block is #10 steel. The materials of the coil and track are copper and #70 Mn steel, respectively [9].

The directions along the length and width of ETB are in accordance with the longitudinal and lateral direction of track, respectively. The longitudinal length and height of the magnet track brake are limited to the bogie size because ETB is installed under the train bogie. Considering the bogie wheel base and the wheel diameter of electric motor train unit, which are 2500 and 860 mm [9], respectively, the longitudinal length of ETB is determined as 1400 mm, which is the basic design condition for the following designs.

### 2.1. Iron Core Parameters

Considering that the largest effective width of the track is 73 mm [10], the width of the iron core and pole shoe is ascertained as 75 mm to achieve the largest working area through electromagnetic field between pole shoes and track.

As exhibited in Figure 1, the magnetic circuit system and magnetic flux leakage are analyzed when the number of electromagnets is assumed to be six.

According to the magnetic circuit principle, the relationship between \( \phi_a \) and \( \phi_b \) is expressed as

\[
\phi_a = B_a S_a \leq 2\phi_b = 2B_b S_b, \tag{1}
\]

where \( \phi_a \) is the magnetic flow through the iron core, \( Wb \); \( \phi_b \) is the magnetic flow through track, \( Wb \); \( B_a \) is the saturation flux density of the electromagnet in point \( a \), \( T \); \( B_b \) is the saturation flux density of track in point \( b \), \( T \); \( S_a \) is the electromagnet cross-sectional area, \( \text{mm}^2 \); and \( S_b \) is the rail cross-sectional area, which equals 7800 mm\(^2\) [10]. According to B-H curves of #10 steel and #70 Mn steel in Figure 2 [11], \( B_a \) is 1.35 T, and \( B_b \) is 1.15 T. The iron core length \( D_1 \) satisfies the following constraint:

\[
D_1 = \frac{2B_b S_b}{75B_a} = 177.2 \text{ mm}. \tag{2}
\]

The final iron core length will be determined later through electromagnet optimization, and it must satisfy the abovementioned constraint equation.

### 2.2. Calculation of Equivalent Air Gap

Equivalent air gap between pole shoe and track is decided after the excitation ampere-turn of coil is designed. Two kinds of air gap present during the operation of the ETB: the air gap between longitudinal beam and iron cores, which is due to the manufacturing process, and the air gap between pole shoes and track, which is caused by track irregularity, real-time contact status, and track contaminants, among others. For a brief calculation, the following assumptions are made.

1. The equivalent air gap equals the sum of the abovementioned air gaps, and it is located between pole shoes and track.
2. The distance from the lowermost portion of pole shoes to the uppermost portion of track equals 1 mm [9]

As shown in Figure 3, the top curve of the lateral cross section of a track is a combinational arc. The half curve mainly consists of Arcs AB, BC, and CD whose radius is 300, 80, and 13 mm, respectively [10]. If the coordinate origin is chosen as represented in Figure 3, the coordinates of points \( A, B, C, \) and \( D \) and the three centers of Arcs AB, BC, and CD can be determined as listed in Table 1. Here, \( \delta_{ab} \) is the distance between the pole shoe bottom and track top, which equals 1 mm.

The magnetic induction is a variable due to the alterable gap between pole shoe and track. The air gap between pole shoe and track can be divided with a great number of magnetic tubes. The magnetic induction in these tubes can be considered equivalent when the magnetic tubes are sufficiently small. The magnetic permeability in one tube is expressed as
\[ G_{AB} = \mu_0 b \int_{X_A}^{X_B} \left( Y_{AB} - \frac{X_{AB}}{X_{AB}} \right) \left( R_2^2 - (x - X_{AB})^2 \right)^{-1} dx \]

\[ G_{BC} = \mu_0 b \int_{X_B}^{X_C} \left( Y_{BC} - \frac{X_{BC}}{X_{BC}} \right) \left( R_2^2 - (x - X_{BC})^2 \right)^{-1} dx \]

\[ G_{CD} = \mu_0 b \int_{X_C}^{X_D} \left( Y_{CD} - \frac{X_{CD}}{X_{CD}} \right) \left( R_2^2 - (x - X_{CD})^2 \right)^{-1} dx \]

where \( X_A, X_B, X_C \), and \( X_D \) are the x-coordinates of Points A, B, C, and D; \( (X_{AB}, Y_{AB}), (X_{BC}, Y_{BC}) \), and \( (X_{CD}, Y_{CD}) \) are the center coordinates of Arcs AB, BC, and CD, respectively. The equivalent air gap between pole shoes and track can be written as

\[ l_{mg} \approx \mu_0^2 \left( \frac{S_e}{2(G_{AB} + G_{BC} + G_{CD})} \right) \]

\[ l_{pg} \approx l_{mg} \]

where \( l_{mg} \) (\( l_{pg} \)) is the equivalent air gap between pole shoes and track. According to Table 1 and equations (3)–(5), the calculation result of \( l_{mg} \) (\( l_{pg} \)) is 1.9 mm.
2.3. Preliminary Design of Magnetic Circuit Coil. The magnetic circuits are excited longitudinally by electromagnets. The network topology scheme of magnetic circuits is depicted in Figure 4. 

when the electromagnet number equals \( n \), there are \((n + 1)\) branch magnetic circuits of the longitudinal beam \( b_{\text{bk}} \) \((1 \leq \kappa \leq n + 1)\), \( n \) branch magnetic circuits of the iron cores \( b_{\text{bk}} \) \((1 \leq \kappa \leq n)\), two branch magnetic circuits of the protection blocks \( b_{\text{pk}} \) \((1 \leq \kappa \leq 2)\), \( n \) branch magnetic circuits of the excitation coils \( b_{\text{ek}} \) \((1 \leq \kappa \leq n)\), \( n \) branch magnetic circuits of the air gaps between pole shoes and track \( b_{\text{mgk}} \) \((1 \leq \kappa \leq n)\), two branch magnetic circuits of the air gaps between protection blocks and track \( b_{\text{pqk}} \) \((1 \leq \kappa \leq 2)\), \((n + 1)\) branch magnetic circuits of track \( b_{\text{h}} \) \((1 \leq \kappa \leq n + 1)\), and \((n + 1)\) loop magnetic circuits \( i_{k} \) \((1 \leq \kappa \leq n + 1)\). The excitation equation of the second magnetic circuit, which consists of two electromagnets, is expressed as

\[
\frac{1}{2} (IW + IW) = \frac{B_{a2}L_{a2}}{\mu_{a2}} + \frac{B_{c2}L_{c2}}{\mu_{c2}} + \frac{B_{\text{mg}}L_{\text{mg}}}{\mu_{0}} + \frac{B_{2}L_{2}}{\mu_{2}} + \frac{B_{\text{mg}}L_{\text{mg}}}{\mu_{0}} + \frac{B_{1}L_{1}}{\mu_{1}} + \frac{B_{c1}L_{c1}}{\mu_{c1}} \tag{6}
\]

where \( I \) is the excitation coil current, \( A; \) \( W \) is the excitation coil number of turns; \( B_{a2}, B_{c2}, B_{\text{mg2}}, B_{2}, B_{\text{mg1}}, \) and \( B_{1} \) is the magnetic induction; \( \mu_{a2}, \mu_{c2}, \mu_{0}, \mu_{2}, \) and \( \mu_{c1} \) is the magnetic permeability, \( H/m; \) and \( L_{a2}, L_{c2}, L_{\text{mg}}, L_{2}, L_{1}, \) and \( L_{c1} \) is the magnetic path length, mm. As air permeability is much smaller than the permeability of \#10 steel and \#70 Mn steel (Wan, 2013), equation (6) can be simplified as

\[
IW > \frac{2B_{\text{mg}}L_{\text{mg}}}{\mu_{0}} = 2 \times 0.0019 \times 1.25 \times 10^{-6} \times B_{\text{mg}} = 3040B_{\text{mg}}. \tag{7}
\]

According to Figure 2, both \#10 steel and \#70 Mn steel B-H curves nearly reach saturation points when \( B = 1.4T \). Hence, \( IW \) should be larger than 4256 ampere-turns. Here, we chose \( IW \) as 5000 ampere-turns by assuming the worst scenario.

A coil arrangement form that intertwines three-layer coils on one iron core is proposed. The circuit of three-layer coils is a parallel circuit; therefore, track brake can supply 72 V as power supply, which is equivalent to the effect of series connection on the iron core. The winding thickness \( b_{k} \) is calculated as [11]:

\[
b_{k} = \sqrt{\frac{\rho_{130} |I/W(3)|^{2}}{2 \eta_{\text{em}} f_{k} \cdot \theta \cdot \beta^{2}}} = \sqrt{\frac{0.02339 \times 1675^{2}}{20 \times 0.001289 \times 0.7 \times 90 \times 3^{2}}} = 16.49 \text{mm}, \tag{8}
\]

where \( \rho_{130} \) is the specific coil coefficient of resistance when the temperature is 130 C, \( \Omega \cdot \text{mm}^{2}/\text{m}; \) \( \eta_{\text{em}} \) is the coil heat dissipation coefficient, W/cm²°C; \( f_{k} \) is the filling coefficient of coil; \( \theta \) is the temperature rise of coil, °C; and \( \beta \) is the depth-width ratio of coil. We ascertain \( b_{k} \) as 16 mm. The current density of \( j \) is selected as 3.5 A/mm² according to the electromagnet design manual. Then, the preliminary sectional area of a single-layer coil \( Q_{k} \) is calculated as

\[
Q_{k} = \frac{IW}{3 \times f_{k}} = \frac{5000}{3 \times 3.5 \times 0.7} = 680.3 \text{ mm}^{2}. \tag{9}
\]

The preliminary height of single-layer coil \( h_{k} \) is calculated as

\[
h_{k} = \frac{Q_{k}}{b_{k}} = \frac{680.3}{16} = 42.5 \text{ mm}. \tag{10}
\]

Therefore, the preliminary height of the single-layer coil is determined as 43 mm. The iron core height is ascertained as 160 mm, which has enough space to twine three-layer coils, and the pole shoe height is ascertained as 20 mm.

The gap between adjacent electromagnets \( l_{\text{em}} \) is 5 mm, and the gap between the protection block and the adjacent electromagnet \( l_{\text{pm}} \) is 2.5 mm, which serves as a safety gap. To guarantee the functions of protection and cleaning, the length, width, and height of the protection block are set as 100, 120, and 180 mm, respectively. The length, width, and height of the longitudinal beam are 1400, 125, and 75 mm, respectively, which can ensure its functions of protection and installing.

Series-wound coil is concatenated in the primary loop, and it requires few windings. For this reason, the series-wound coil with \( H \) skeleton is selected. The thickness of the coil framework is 3 mm. Considering that a considerable amount of heat is generated by rubbing between pole shoes and track, the rank of the coil insulation is selected with an \( H \) shape. Moreover, insulating resin is placed between the coil and the iron core for insulation. The thickness of the insulating resin and the electromagnet shell is 2 and 1.5 mm, respectively.

In sum, the adjacent iron core gap \( l_{\text{aic}} \) is 50 mm, and the gap between the protection block and the adjacent iron core \( l_{\text{pic}} \) is 25 mm.

3. Simulation and Optimization

We conduct the optimization of ETB through simulation. First, the theoretical basis of electromagnetic field analysis is illustrated. Then, the assumptions of a finite element model and its simulation results are demonstrated. Finally, optimizations of the number of electromagnets and the pole shoe gap are presented.

| \( X (\text{mm}) \) | \( A \) | \( B \) | \( C \) | \( D \) | Center of arc AB | Center of arc BC | Center of arc CD |
|-----------------|------|------|------|------|----------------|----------------|----------------|
| \( Y (\text{mm}) \) | \( \delta_{ab} \) | \( \delta_{ab} + 0.2 \) | \( \delta_{ab} + 2.2 \) | \( \delta_{ab} + 14.2 \) | 0 | 7.387 | 22.417 |

| \( \delta_{ab} + 300 \) | \( \delta_{ab} + 80.157 \) | \( \delta_{ab} + 14.865 \) |}

---

**Table 1:** Coordinates needed in calculating equivalent air gap.
3.1. Theoretical Basis of Electromagnetic Field Analysis.

Numerical analysis of an electromagnetic field involves solving Maxwell equations and other partial differential equations under the given boundary conditions.

The induced electromotive force in a closed loop is proportional to the change rate of magnetic flux through the circuit, which is given as

\[ \oint \vec{E} \cdot d\vec{l} = -\iint_{\Omega} \frac{\partial \vec{B}}{\partial t} \cdot d\vec{S}, \quad (11) \]

where \( \vec{E} \) is the electric field intensity, \( \text{V/m} \).

The electric flux, which passes through any closed surfaces, equals the electric charge quantity encapsulated by the closed surfaces regardless of the distribution of electrolyte and electric flux density in the electric field. The electric flux can be expressed as

\[ \iint_S \vec{D} \cdot d\vec{S} = \iiint_V \rho_1 \, dV, \quad (12) \]

where \( \rho_1 \) is the electric charge volume density, \( \text{C/m}^3 \), and \( V \) is the volume area surrounded by closed surfaces.

The line integral of magnetic field intensity along any closed path equals the total current that passes through the hook face, which is determined through this integral path as

\[ \oint \vec{H} \cdot d\vec{l} = \iiint_{\Omega} \left( \vec{j} + \frac{\partial \vec{D}}{\partial t} \right) \cdot d\vec{S}, \quad (13) \]

where \( \vec{j} \) is the density vector of the conduction current; \( \partial \vec{D}/\partial t \) is the displacement current density, \( \text{A/m}^2 \); and \( \vec{D} \) is electric flux density, \( \text{C/m}^2 \).

The magnetic flux that passes through any closed surface equals zero regardless of the distribution of magnetic flux density vector and medium, which is shown as follows:

\[ \iint_S \vec{B} \cdot d\vec{S} = 0. \quad (14) \]

Several physical and engineering parameters are required when solving engineering electromagnetic field problems. Therefore, knowledge of the energy storage of the electric field, the magnetic flux density, the magnetic flux, and calculation of electromagnetic force, and torque is required. The parameters are derived from electric potential and magnetic potential relationships as

\[ Q = \frac{\epsilon}{2} \int_{\Omega} |\nabla \phi|^2 \, d\Omega = \frac{\epsilon}{2} \sum_{i=1}^{n} \int_{\Omega^i} \left( \frac{\partial \phi}{\partial x} \right)^2 + \left( \frac{\partial \phi}{\partial y} \right)^2 + \left( \frac{\partial \phi}{\partial z} \right)^2 \, d\Omega, \quad (15) \]

where \( Q \) is the energy source term. The energy storage of the electric field can be obtained if the electric field of the electric potential is calculated according to equation (15). The finite element method to achieve total field energy by summing up all unit energies can be expressed as

\[ B = \nabla \times \vec{A} = x \frac{\partial A}{\partial y} - y \frac{\partial A}{\partial x}, \quad (16) \]

where \( A \) is the vector of magnetic potential. Magnetic field power is often expressed by magnetic flux density, \( B \), which is calculated by directional derivative of potential function. The magnetic flux can be obtained by the surface integral of the magnetic flux density as

\[ \phi_m = \iint_S B \, dS = \iint_S \nabla \times \vec{A} \cdot d\vec{S}. \quad (17) \]

Electromagnetic force can be achieved by using virtual displacement after energy storage of electric field through potential function is obtained. Virtual displacement replaces the differential quotient with a difference quotient. Moreover, it calculates magnetic variation to confirm electromagnetic force and electromagnetic torque as follows:

\[ F = \frac{\partial W_m}{\partial \vec{s}} = \frac{\partial W_{m1}}{S_1 - S_0}, \quad (18) \]

\[ T_m = P \frac{\partial W_m}{\partial \theta} = P \frac{\partial W_{m1}}{\theta_1 - \theta_0}, \quad (18) \]

where \( W_{m0} \) is the magnetic energy before virtual displacement; \( W_{m1} \) is the magnetic energy after virtual displacement; \( \theta_0 \) and \( S_0 \) is the location of model before virtual displacement; \( \theta_1 \) and \( S_1 \) is the location of model after virtual displacement.

3.2. Finite Element Model. Finite element simulation of ETB is developed by using a three-dimensional (3D) model to investigate EAF and magnetic field distribution [12]. For the analysis of the present model, the following assumptions are made:

![Figure 4: Network topology scheme of magnetic circuits.](image-url)
(1) The process is steady and isothermal
(2) The model is three-dimensional, and it depends on x, y, and z directions
(3) Adjacent electromagnet current has reverse directions
(4) Waterproof layer, shell, and other structures are ignored because they have little influence on the electromagnetic field [9]
(5) The natural boundary condition and Neumann boundary condition are applied for the model
(6) The ideal air gap between pole shoes and the track is 1 mm
(7) The number of electromagnets is assumed to be six

Ansoft Maxwell is finite element software that specializes in electromagnetic simulation, and it uses electromagnetic field information to predict product performance accurately from physical design information. The software can automatically develop a grid partition. However, some meshes are added manually to increase magnetic field accuracy. According to partition methodology, a refined mesh is carried out in the contact zone to achieve EAF and magnetic distribution precisely. The gridding is composed of four-node tetrahedral finite elements, and the mesh generation parameters are presented in Table 2.

As depicted in Figure 5, a very fine mesh is employed to achieve desired results, which can meet the accuracy of finite element analysis.

3.3. Simulation Results. The convergence results are exhibited in Table 3. The relationships among number of convergence and triangle unit, total energy, and energy error are illustrated intuitively in the table.

As shown in Figure 6, the various colors represent different magnetic field intensities. The color of pole shoes is red, which indicates a large magnetic flux density. The magnetic field gradually strengthens as one move closer to the pole shoe gap because of looping-in that develops between adjacent magnets.

Figure 7 shows the magnetic flux density distribution of a track surface. The six red rectangular blocks correspond to each of the six pole shoes; red, yellow, green, and blue areas primarily exist. The contact areas between pole shoes and track are red, which indicates strong magnetic flux density. The magnetic flux density of other areas gradually weakens the farther one is from pole shoes. Figure 8 shows the magnetic flux density distribution of the bottom of pole shoes, whose distribution rules are similar to those showed in Figure 7.

We obtain different EAFs by setting different current excitations. As shown in Table 4, the EAF is greater when ampere-turn is added. However, the EAF increases very little when the current excitation is more than 5000 ampere-turns, which means that the force has nearly reached the limit. Hence, the choice of 5000 ampere-turns as the current excitation is a reasonable decision.

3.4. Optimization of ETB. The electromagnet number and the pole shoe gap are optimized in this part to improve the EAF between ETB and track by using Ansoft Maxwell.

Different EAFs are achieved with the variation of magnet number when the effective air gap between pole shoes and track is 1 mm. The current excitation of coil varies at 1630, 3300, and 5000 A, respectively. As shown in Table 5, EAF is at its maximum when the magnet number is six. However, the magnetic circuit number will decrease as the electromagnet length increases. Moreover, decreased electromagnet length will lead to a serious decline in single magnetic flux [5, 13].

The gap between adjacent pole shoes has a certain influence on EAF. The leakage flux will increase if the gap is too small. However, the working area between pole shoes and track will reduce when the gap is too large, which will decrease the main flux [5, 13]. Thus, the gap has an optimum value when the electromagnet is determined.

Table 6 shows the relationship between the pole shoe gap and EAF when a 10 mm step change of the pole shoe gap is used. EAF reduces when the pole shoe gap is more than 40 mm due to the decrease in the effective friction area between pole shoes and track. EAF reduces when the pole shoe gap is less than 40 mm because the leakage flux between adjacent pole shoes increases. Therefore, the gap between adjacent pole shoes is determined as 40 mm.

4. Final Design of ETB Based on the Optimizations

The final design of ETB based on the optimization results is obtained in this section. The iron core length is determined by ascertaining six electromagnets. The copper wire diameter, coil turns, and the height of the single-layer coil are calculated based on iron core length. Then, the integrated parameters of ETB are presented.

4.1. Design of Magnetic Circuit Coil Based on Optimizations. The iron core length \( D_1 \) is 150 mm when the magnet number is six, which satisfies the constraint equation (2). Then, we can confirm the average diameter of coil as

\[
D_{cp} = \frac{D_1 + f}{2} + b_k = \frac{150 + 75}{2} + 16 = 128.5 \text{ mm} \quad (19)
\]
Table 3: Convergence data.

| Pass | # Tetrahedra | Total energy (%) | Energy error (%) | Delta energy (%) |
|------|--------------|------------------|------------------|-----------------|
| 1    | 273,788      | 509.81           | 23.168           | N/A             |
| 2    | 355,874      | 478.66           | 5.0929           | 0.91799         |
| 3    | 462,674      | 474.27           | 3.0581           | 0.32446         |
| 4    | 601,462      | 470.41           | 1.2327           | 0.06139         |

Figure 5: Grid partition model.

Figure 6: Vector magnetic flux density.

Figure 7: Magnetic flux density on the track surface.

Figure 8: Magnetic flux density on the pole shoes surface.
As magnetic potential is generated when the current passes through the coil winding, the equations of voltage and magnetic potential are expressed as follows (Wan, 2013):

\[ q = \frac{\pi d^2}{4} \]
\[ R = \frac{4\rho D_{cp} W}{q} \]
\[ U = IR = \frac{1W}{W} \frac{4\rho D_{cp} W}{q} = \frac{16\rho D_{cp} IW}{\pi d^2} \]  \hspace{1cm} (20)

where \( U \) is the supply voltage, \( V \); \( R \) is the field coil resistance, \( \Omega \); \( \rho \) is the coil coefficient of resistance, \( \Omega \cdot \text{mm}^2/\text{m} \); \( D_{cp} \) is the mean diameter of excitation coil, \( m \); and \( q \) is the cross-sectional area of bare copper wire, \( \text{mm}^2 \). The copper wire diameter can be calculated according to equation (20) as

\[ d = \sqrt{\frac{16\rho D_{cp} IW}{\pi U}} = \sqrt{\frac{16 \times 0.02339 \times 0.1285 \times 1675}{3.14 \times 24}} = 1.0339 \text{ mm}. \]  \hspace{1cm} (21)

The copper wire diameter \( d \) is determined as 1.04 mm, and the outer diameter of enamelled wire \( d_1 \) is chosen as 1.12 mm according to the enameled wire coil specification table [11]. Electromagnet coil calorific value is an important factor in electromagnet design. Furthermore, the maximum temperature of coil must be under the allowable value [14].

\[ \theta = \frac{p}{\mu_n S} = \frac{U^2}{R \mu_n S} \]
\[ S = S_H + \eta_n S_B \]  \hspace{1cm} (22)

where \( p \) is the coil power, \( W \); \( S \) is the heat dissipating area, \( \text{mm}^2 \); \( S_H \) is the outer surface area of the coil, \( \text{mm}^2 \); and \( \eta_n \) is the coil factor, \( \text{mm}^2 \). The heat radiating area \( S \) and the coil resistance \( R \) can be calculated according to equation (22).

\[ S = S_H + \eta_n S_B = (75 + 150 + 16 \times 4) \times 2 \times 45 + 2 \]
\[ \times (75 + 150) \times 2 \times 45 = 66510 \text{ mm}^2, \]  \hspace{1cm} (23)

\[ R \geq \frac{U^2}{\mu_n S \theta} = \frac{24 \times 24}{0.001204 \times 665.1 \times 90} = 7.99 \Omega. \]

\( R \) is ascertained as 8.5 \( \Omega \). Moreover, \( I \) and \( W \) are confirmed as follows:

\[ I = \frac{U}{R} = \frac{24}{8.5} = 2.8 \text{ A.} \]  \hspace{1cm} (24)
\[ W = \frac{1W}{I} = \frac{1675}{2.8} = 600 \text{ Turns.} \]  \hspace{1cm} (25)

The calorific value of the coil should be limited to ensure that the current density value meets certain requirements. Therefore, the current density value of the coil is obtained as

\[ j = \frac{I}{q} = \frac{4 \times 2.8}{3.14 \times 1.04^2} = 3.3 \text{ A/mm}^2. \]  \hspace{1cm} (26)

The current density value satisfies the electromagnet design requirement for uninterrupted operation [14]. The filling coefficient of the coil, the coil sectional area, and the coil height are calculated as follows:

\[ f_k = \frac{\pi}{4} \left( \frac{d}{d_1} \right)_k = \frac{3.14}{4} \times \left( \frac{1.04}{1.12} \right)^2 = 0.68, \]
\[ Q_k = \frac{q \times W}{f_k} = \frac{0.849 \times 600}{0.68} = 749.1 \text{ mm}^3; \]  \hspace{1cm} (28)
\[ h_k = \frac{Q_k}{b_k} = \frac{749.1}{16} = 46.8 \text{ mm}. \]

Therefore, the final height of the single-layer coil is designed as 47 mm. The three-layer coils of one electromagnet can supply 5040 ampere-turns according to

\begin{table}[h]
\centering
\caption{Relationship between ampere-turns and attractive force.}
\begin{tabular}{|c|c|c|c|c|c|}
\hline
Coil excitation (ampere-turn) & 1630 & 3300 & 5000 & 6000 \\
\hline
Attractive force (N) & 39,722 & 50,181 & 61,401 & 62,397 \\
\hline
\end{tabular}
\end{table}

\begin{table}[h]
\centering
\caption{Attractive force at different electromagnet number and current excitation.}
\begin{tabular}{|c|c|c|c|c|c|c|}
\hline
Current excitation (ampere-turn) & Four magnets & Five magnets & Six magnets & Seven magnets & Eight magnets \\
\hline
1630 & 20,899 & 28,404 & 39,722 & 37,522 & 32,350 \\
3300 & 26,402 & 35,883 & 50,181 & 47,401 & 40,860 \\
5000 & 32,305 & 43,906 & 61,401 & 58,032 & 50,152 \\
6000 & 34,419 & 45,465 & 62,397 & 58,904 & 50,442 \\
\hline
\end{tabular}
\end{table}

\begin{table}[h]
\centering
\caption{Relationship between pole shoe gap and attractive force.}
\begin{tabular}{|c|c|c|c|c|c|}
\hline
Pole shoe gap (mm) & 50 & 40 & 30 & 20 & 10 \\
\hline
Attractive force (N) & 60,728 & 61,401 & 60,751 & 58,116 & 56,542 \\
\hline
\end{tabular}
\end{table}
4.2. Integrated Design of ETB. Considering the above-mentioned relations, the thickness of the coil, framework, insulating resin, and the electromagnet shell is 16, 3, 2, and 1.5 mm, respectively. Hence, the width \( w_{em} \) and length \( l_{em} \) of the electromagnet is calculated as follows:

\[
\begin{align*}
    w_{em} &= 75 + 16 \times 2 + 3 \times 2 + 2 \times 2 + 1.5 \times 2 = 120 \text{ mm}, \\
    l_{em} &= 150 + 16 \times 2 + 3 \times 2 + 2 \times 2 + 1.5 \times 2 = 195 \text{ mm}.
\end{align*}
\]

(29)

The parameters of the ETB are illustrated in Table 7.

### 5. Experimental Verification of EAF

We develop a prototype based on optimized parameters. Then, static tests of EAF and a comparison between tests and simulations are carried out. Finally, the electromagnetic BF (EBF) of ETB is calculated in the next section.

#### 5.1. Prototype Manufacture

We develop a 3D model by using CATIA software according to the parameters in Table 7. Figure 9(a) indicates the electromagnet structure, and Figure 9(b) represents the assembly drawing of ETB.

#### 5.2. Attractive Force Test

Figure 10(a) shows a picture of the final prototype assembly. The threaded holes on the top of the longitudinal beam are used to install rings when performing the experiment. The holes on the side face of the longitudinal beam are used to install a suspension system of ETB. Figure 10(b) shows the assembly, where the ETB is connected to an electronic scale through rings and a pendant chain and is lifted up gradually by a traveling crane. Track is fixed on the floor by U-profile steels. The numerical value of EAF and track brake weight can be directly read from an electronic scale when track brake is separated from track. The numerical value of track brake weight is a constant value. Therefore, the EAF is easy to obtain.

#### 5.3. Contrastive Analyses of Tests and Simulations

We develop a prototype based on optimized parameters. Consider the above-mentioned relations, the thickness of the coil, framework, insulating resin, and the electromagnet shell is 16, 3, 2, and 1.5 mm, respectively. Hence, the width \( w_{em} \) and length \( l_{em} \) of the electromagnet is calculated as follows:

\[
\begin{align*}
    w_{em} &= 75 + 16 \times 2 + 3 \times 2 + 2 \times 2 + 1.5 \times 2 = 120 \text{ mm}, \\
    l_{em} &= 150 + 16 \times 2 + 3 \times 2 + 2 \times 2 + 1.5 \times 2 = 195 \text{ mm}.
\end{align*}
\]

The average value of EAF is achieved as the final result through many experiments. The contrastive analyses of tests and simulations are exhibited in Table 8.

The EAF of tests agrees with that of the simulations. The error is within the acceptable range. The following explanations for discrepancies between the test and the simulation are given after careful observations of the test process:

1. Negative factors, such as pits and dust on track surface, have some effect on the experiment result. In addition, the contact between pole shoes and track may be incomplete due to assembly error.
2. The material property of ETB is constant during the simulation, while temperature influences copper wire resistance during the test.
3. The magnetizing curve used in the simulation is referred to as the electrical engineering handbook, whose value is slightly larger than the actual value [11].

### 6. Estimation of EBF

A facility for a dynamic EBF test is unavailable. Therefore, EBF and braking deceleration are estimated by using friction coefficient [15].

As the weight of CRH2 \( M \) is 441,180 kg, its air braking force \( F_{ab} \) is expressed as [14]

\[
F_{ab} = 510170 \times \frac{v + 150}{2v + 150},
\]

(30)

where \( v \) is train speed, km/h. CRH2 has eight carriages, and it can be equipped with 16 ETBs [16]. According to the empirical equation from a Russian Federation laboratory, the friction coefficient of track \( \mu_k \) and the EBF \( F_{2ab} \) are expressed as [17]

| Component         | Parameter                      | Data                        |
|-------------------|--------------------------------|-----------------------------|
| Iron core         | Length × width × height        | 150 mm × 75 mm × 160 mm     |
| Pole shoe         | Length × width × height        | 160 mm × 75 mm × 20 mm      |
|                   | Gap                            | 40 mm                       |
| Coil              | Inner diameter                 | 160 mm × 85 mm              |
|                   | Coil resistance                | 130°C 8.5 Ω                 |
|                   | Room temperature               | 8 Ω                         |
|                   | Height                         | 47 mm × 3                   |
|                   | Thickness                      | 16 mm                       |
|                   | Working voltage                | 24 V                        |
|                   | Magnetic potential             | 1675 × 3 ampere-turns       |
| Electromagnet     | Outer diameter                 | 195 mm × 120 mm             |
|                   | Number                         | 6                           |
|                   | Gap                            | 5 mm                        |
| Protection block  | Length × width × height        | 100 mm × 120 mm × 180 mm    |
|                   | Gap                            | 2.5 mm                      |
| Longitudinal beam | Length × width × height        | 1400 mm × 125 mm × 75 mm    |

Table 7: Parameters of the ETB.
\[ \mu_k = 0.19 \times \frac{10.8v + 100}{21.6v + 100} \quad (31) \]

\[ F_{eb} = 56940 \times 16 \times \mu_k = 173097.6 \times \frac{10.8v + 100}{21.6v + 100} \quad (32) \]

As the running resistance of CRH2 is too small compared with the air BF and the EBF, the braking deceleration of CRH2 \( a_b \) is calculated according to equations (30) and (32) as

\[ a_b = \frac{F_{ab}}{M} + \frac{F_{eb} M}{M} = 1.16 \times \frac{v + 150}{2v + 150} + 0.39 \times \frac{10.8v + 100}{21.6v + 100} \quad (33) \]

The single ETB installed in the German ICE can provide 41,237 N-EAF. When it is used for CRH2, the electromagnetic braking deceleration of CRH2 \( a_{tb} \) is expressed as

\[ a_{tb} = 1.16 \times \frac{v + 150}{2v + 150} + 0.28 \times \frac{10.8v + 100}{21.6v + 100} \quad (34) \]
As shown in Figure 11, the proposed ETB can provide 0.20 m/s² braking deceleration, while ETB for ICE can provide 0.14 m/s² braking deceleration when the train speed is 200 km/h. Therefore, the proposed ETB can enhance braking deceleration by 39% because of its longitudinal magnetic circuit and its functioning.

7. Conclusions

In the present study, a new ETB is proposed that has the following two outstanding characteristics: first, longitudinal-axis magnetic circuits excited by electromagnets with multiple coils, and second, a design in which pole shoes extend outwards. The proposed ETB is optimized to improve the BF, the electromagnet number is optimized to be six, and the pole shoe gap is optimized to be 40 mm. Moreover, experimental verification of electromagnetic attractive force is performed through prototype tests, and the newly developed electromagnetic track brake can enhance electromagnetic braking deceleration by 39%.

Data Availability

The calculated data used to support the findings of this study are included within the article.

Conflicts of Interest

The authors declare that there are no conflicts of interest regarding the publication of this paper.

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