Hydrodynamic modelling of ejecta shrapnel in the Vela supernova remnant

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ABSTRACT
Many supernova remnants (SNRs) are characterized by a knotty ejecta structure. The Vela SNR is an excellent example of remnant in which detached clumps of ejecta are visible as X-ray emitting bullets that have been observed and studied in great detail. We aim at modelling the evolution of ejecta shrapnel in the Vela SNR, investigating the role of their initial parameters (position and density) and addressing the effects of thermal conduction and radiative losses. We performed a set of 2D hydrodynamic simulations describing the evolution of a density inhomogeneity in the ejecta profile. We explored different initial setups. We found that the final position of the shrapnel is very sensitive to its initial position within the ejecta, while the dependence on the initial density contrast is weaker. Our model also shows that moderately overdense knots can reproduce the detached features observed in the Vela SNR. Efficient thermal conduction produces detectable effects by determining an efficient mixing of the ejecta knot with the surrounding medium and shaping a characteristic elongated morphology in the clump.

Key words: hydrodynamics – shock waves – methods: numerical – ISM: individual objects: Vela SNR – ISM: kinematics and dynamics – ISM: supernova remnants.

1 INTRODUCTION
The ejecta in supernova remnants (SNRs) drive the exchange of mass and the chemical evolution of the Galactic medium. The structure of SNR ejecta has been proved to be knotty, and several clumps have been observed at different wavelengths in remnants of core-collapse supernovae (SNe), as G292.0+1.8 (Park et al. 2004), Puppis A (Katsuda et al. 2008) and Cas A, where knots have been observed also beyond the main shock front (Fesen et al. 2006; Hammell & Fesen 2008; DeLaney et al. 2010).

The Vela SNR, being the nearest SNR, represents a privileged target for this kind of studies, since it is possible to observe fine structures down to small physical scales. Despite the bulk of the X-ray emission of the Vela SNR is associated with the post-shock interstellar medium, X-ray emitting ejecta have also been observed. In particular, six protruding features, with characteristic boomerang morphology, (labelled Shrapnel A–F) have been identified in the Vela SNR by Aschenbach, Egger & Trumper (1995), who argued an ejecta origin for these structures which appear to be detached from the remnant. The association with ejecta fragments has been supported by more recent observations performed with Chandra, XMM–Newton and Suzaku. The analysis of the XMM–Newton observation of Shrapnel D has revealed that O, Ne and Mg abundances are significantly larger than solar (Katsuda & Tsunemi 2005). A similar abundance pattern has been observed with Suzaku in Shrapnel B (Yamaguchi & Katsuda 2009), but in this case the overabundances of the lighter elements are less prominent, suggesting more effective mixing with the interstellar medium (ISM). A Chandra observation of Shrapnel A, whose projected distance from the centre of the remnant is larger by ~20 per cent than Shrapnel D, reveals instead oversolar Si:O ratios (Miyata et al. 2001). Significant Si overabundance (Si ~3) has been confirmed by Katsuda & Tsunemi (2006), who analysed an XMM–Newton observation, finding solar or subsolar values for the O, Ne, Mg and Fe abundances. These results show differences in the chemical composition between Shrapnel A and Shrapnel B and D. In the northern rim of the Vela shell, Miceli, Bocchino & Reale (2008) discovered new X-ray emitting clumps of ejecta whose projected position is behind the main shock front. The relative abundances (O:Ne:Mg:Fe) of these new shrapnel are in good agreement with those observed in Shrapnel D. Similar abundance pattern have been observed also by LaMassa, Slane & de Jager (2008), who found ejecta-rich plasma in the direction of the Vela X pulsar wind nebula.

The present day morphology of SNRs and the structure of ejecta are believed to reflect the physical characteristics of the SN explosion (e.g. intrinsic asymmetries of the explosion, interaction of the early blast with the inhomogeneities of the circumstellar medium).
physical processes in the aftermath of the explosion, etc.) and their detailed study promises to contribute to our understanding of the SN explosion physics. In the light of these considerations, it is then interesting to model the evolution of the ejecta knots to understand how the current position and chemical properties of the shrapnel in the Vela SNR depend on the physical conditions at the SN explosion and on the dynamics of the explosion itself.

The evolution of dense, supersonic clumps of SN ejecta running in a uniform medium has been studied by Anderson et al. (1994) and Jones, Kang & Tregillis (1994), who identified three main stages of evolution: a bow-shock phase, an instability phase and a dispersal phase. However, these models do not describe in detail the interaction of the clump with the remnant (post-shock medium, main shock, reverse shock) and do not include important physical effects (as thermal conduction and radiative cooling). Cid-Fernandes et al. (1996) included radiative losses in their 2D models, but they focused on the interaction of a knot with a very small SNR ($\sim 10^{17}$ cm, i.e. more than 100 times smaller than the Vela SNR) evolving in an extremely dense medium ($10^7$ cm$^{-3}$). A hydrodynamic model (without thermal conduction and radiative cooling) specifically tuned for the Vela SNR has been developed by Wang & Chevalier (2002, hereafter WC02) who followed the evolution of a shrapnel by using 2D simulations in spherical coordinates (because of the geometry of their simulations, the shrapnel are modelled as toroidal structures with very large masses). WC02 did not model the early evolution of the ejecta knot, but started their simulations at the time $t_{inv}$ corresponding to the first interaction of the shrapnel with the reverse shock front. They explored different values of $t_{inv}$ and of the density contrast between the shrapnel and the surrounding ejecta, $\chi$, and found that, in order to produce an observable protrusion on the shock front (like that observed in Shrapnel A–F), a very high density contrast ($\chi \sim 1000$) is necessary. With lower density contrasts ($\chi < 100$), the shrapnel are rapidly decelerated and fragmented by hydrodynamic instabilities and the observed features cannot be reproduced (for the effects of hydrodynamic instabilities on shocked clouds see also Klein, McKee & Colella 1994; Orlando et al. 2005). Large density inhomogeneities in the clumps are difficult to explain in a core-collapse SN explosion. WC02 argued that a model that includes the effects of radiative cooling may show that lower values of $\chi$ are needed to match the observed protrusions. Also, WC02 do not include in their model the effects of thermal conduction that, as shown by Orlando et al. (2005), can efficiently suppress the hydrodynamic instabilities, thus allowing the shrapnel to overcome the main shock front without being disrupted. Recently, the evolution of knotty ejecta in a Type Ia SNR has been modelled by Orlando et al. (2012, hereafter O12), who found that small clumps with initial $\chi < 5$ can reach the SNR shock front after $\sim 1000$ yr. Nevertheless, these ejecta knots are then rapidly eroded and do not produce significant protrusions in the SNR shock front, thus being unable to reproduce the features observed in the Vela SNR.

Here we present a set of 2D hydrodynamic simulations of the evolution of an (initially spherical) ejecta shrapnel in the Vela SNR. We include in our model both thermal conduction and radiative cooling and explore different values of $\chi$ and of the initial position of the shrapnel in the ejecta profile. We aim at addressing the role of thermal conduction and radiative cooling and at understanding how the initial properties of the shrapnel influence its evolution. We also aim at evaluating whether values of $\chi$ lower than 100 ($\chi = 10–50$) can reproduce the observed features.

The paper is organized as follows: the hydrodynamic model is described in Section 2, the results of the simulations are shown in Section 3, and our conclusions are discussed in Section 4.

2 HYDRODYNAMIC MODELLING

2.1 Initial conditions and model equations

We model the evolution of a shrapnel in a SNR by performing a set of 2D simulations in a cylindrical coordinate system ($r, \theta, z$), assuming axial symmetry. The system setup consists of a spherically symmetric distribution of ejecta with initial kinetic energy $K = 10^{51}$ erg (the initial thermal energy is only the 0.2 per cent of $K$) and mass $M_{ej} = 12 M_\odot$ (representing the initial blast wave), where we place a dense, spherical knot (the shrapnel) in pressure equilibrium with the surrounding ejecta and with central coordinates $(0, R_s)$.

The radial density profile of the ejecta consists of two power-law segments ($\rho \propto r^{-m}$ on the inside and $\rho \propto r^{-b}$ on the outside), in agreement with the density structure in a core-collapse SN described by Chevalier (2005). For our simulations, we use $m = 1$ and $b = 11.2$, and the position of the transition between the flat and steep regimes is derived by following Chevalier (2005). The initial velocity of the ejecta increases linearly (up to $6 \times 10^8$ cm s$^{-1}$) with their distance from the centre. The maximum velocity is reached at the initial radius of the ejecta, i.e. $R_{ej}^0 = 4.5 \times 10^{18}$ cm. These values correspond to $\sim 240$ yr after the explosion, appropriate for the relatively late stages of the SNR evolution that we address in this study. In fact, the starting time of our simulations corresponds to only $\sim 2$ per cent of the Vela SNR age and the shrapnel reaches the reverse shock $\sim 2500$–3000 yr after the explosion in all our simulations (i.e. the system has enough time to evolve, before the interaction of the shrapnel with the SNR reverse shock occurs). We then conclude that our simulations can provide a realistic description of the actual conditions in the Vela SNR.

The initial mass of the shrapnel is $0.05 M_{ej} (1.19 \times 10^{33}$ g), its density is $\chi$ times larger than that of the surrounding ejecta at distance $R_s$ from the centre and its velocity is the same as that of the ejecta at distance $R_s$ from the centre. We aim at showing that the detached shrapnel observed in the Vela SNR can be the result of moderately overdense clumps of ejecta originating in relatively internal layers. We explored different values of $\chi$ and $R_s$, namely $\chi = 10, 20, 50$ and $R_s = 1/6 R_{ej}^0, 1/3 R_{ej}^0, 1/2 R_{ej}^0$. Fig. 1 shows the initial density and temperature conditions for the case with $\chi = 20$ and $R_s = 1/3 R_{ej}^0$. The simulation setups discussed in this paper are summarized in Table 1.

Vela SNR is the result of a core-collapse SN and we expect the ambient medium to be ‘perturbed’ by the wind residuals of the massive progenitor star. However, we assume for simplicity a uniform ambient medium as in WC02, since here we are not interested in modelling the details of the remnant evolution. The final (i.e. after $11,000$ yr, the age of the Vela SNR; Taylor, Manchester & Lyne 1993) radius of the remnant strongly depends on the choice of the ambient density value, $n_{SSM}$. We set $n_{SSM} = 0.5$ cm$^{-3}$, because with this value (and with the chosen values of $K, M_{ej}, n_{SSM}, b$ and $m$), the radius of the shell after $11,000$ yr is $R_{shell} \approx 5.4 \times 10^{19}$ cm, in good agreement with the observed radius of the Vela SNR that ranges between $5 \times 10^{19}$ and $5.5 \times 10^{19}$ cm (by assuming a distance of $250$ pc, in agreement with Bocchino, Maggio & Sciortino 1999 and Cha, Sembach & Danks 1999).

Our model solves the time-dependent compressible fluid equations of mass, momentum and energy conservation. In three cases, we ran the same simulation with/without thermal conduction and radiative cooling and explored different values of $\chi$ and of the initial position $t_{inv}$ of the shrapnel.

1 The size of the clump varies accordingly.
radiative cooling inside our system, as shown in Table 1. As for thermal conduction, we considered both the Spitzer and the saturated regimes, while radiative losses (that can play an important role in the Vela SNR, as shown by Miceli et al. 2006) were computed for an optically thin thermal plasma. The model equations are described in Miceli et al. (2006, equations 1–5 therein) and were solved by using the FLASH code (Fryxell et al. 2000).

The computational domain extends over $8 \times 10^{19}$ cm in the $r$ and $z$ directions. We use axisymmetric boundary conditions at $r = 0$, reflection boundary conditions at $z = 0$ and zero-gradient (outflow) boundary conditions (for $v$, $\rho$, and $p$) elsewhere. We trace the motion of the ejecta material and of the shrapnel with passive tracers.\(^2\) Considering the large range in spatial scales of our simulations, we exploited the adaptive mesh capabilities of the FLASH code by adopting up to 10 nested levels of resolution (the resolution increases by a factor of 2 at each level). The refinement/derefinement criterion (Lohner 1987) follows the gradients of density, temperature and tracers. The finest spatial resolution is $1.95 \times 10^{16}$ cm at the beginning of the simulation, therefore there are 230 computational cells per initial radius of the ejecta and $\sim 10$ cells per initial radius of the shrapnel (that varies in the range $1.8\text{–}2.9 \times 10^{12}$ cm). Because of the expansion of the system, the resolution is reduced by a factor of 20 times denser than the surrounding ejecta.

Both tracers have zero mass and do not modify the dynamics of the system.\(^2\)

![Figure 1](http://mnras.oxfordjournals.org/) Density (left-hand panel) and temperature (right-hand panel) 2D cross-sections through the $(r, z)$ plane showing an example of the initial conditions of our simulations (namely $R1/3 - CH120$, see Table 1). The system consists of an expanding spherically symmetric distribution of ejecta where we place a dense, isobaric and spherical knot. In this case the knot is 20 times denser than the surrounding ejecta.

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Table 1. Physical parameters of the model setups (see Section 2). TC-RL indicates that the simulations were performed by including thermal conduction and radiative losses. In all the setups the initial radius of the ejecta is $R_{\text{eq}} = 4.5 \times 10^{18}$ cm.

| Model setup        | $\chi$ | $R_1$ (cm) | TC-RL |
|--------------------|--------|------------|-------|
| $R1/3 - CH110$     | 10     | $1.5 \times 10^{18}$ | No    |
| $R1/3 - CH110 - TR$| 10     | $1.5 \times 10^{18}$ | Yes   |
| $R1/3 - CH120$     | 20     | $1.5 \times 10^{18}$ | No    |
| $R1/3 - CH120 - TR$| 20     | $1.5 \times 10^{18}$ | Yes   |
| $R1/3 - CH150$     | 50     | $1.5 \times 10^{18}$ | No    |
| $R1/6 - CH150$     | 50     | $0.75 \times 10^{18}$ | No    |
| $R1/6 - CH150 - TR$| 50     | $0.75 \times 10^{18}$ | Yes   |

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We first focus on simulation $R1/3 - CH120$. Fig. 2 shows the 2D cross-sections through the $(r, z)$ plane of temperature and density at different evolutionary stages of the $R1/3 - CH120$ simulation. The left-hand panel shows the system 5000 yr after the beginning of the simulation,\(^3\) when the shrapnel interacts with the intershock region. Rayleigh–Taylor and Richtmyer–Meshkov instabilities are visible as finger-like structures both in the density and temperature maps. At this stage, the knot is partially eroded by the hydrodynamic instabilities and evolves towards a core-plume structure. The core of the knot, however, is still significantly overdense with respect to the surrounding shocked ejecta. The right-hand panel of Fig. 2 shows the shrapnel at $t = 11 \times 10^{3}$ yr, with its characteristic supersonic bow shock protruding beyond the SNR main shock.

WC02 found that ejecta knots with density contrast $\chi = 100$ are rapidly fragmented and decelerated in the intershock region and do not even reach the main shock front (these effects being more dramatic for small clumps). Nevertheless, we notice that the value of $\chi$ in WC02 refers to the onset of the interaction between the knot and the reverse shock and that $\chi$ is not constant during the evolution of the system. In the ‘free’ expansion phase, the

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\(^3\) In the following, all the ages will be reckoned from the beginning of our simulations. We remind the reader that our initial condition corresponds to $\sim 240$ yr after the SN explosion.
density of the shrapnel does not drop down uniformly (as that of the other ejecta does) and the shrapnel undergoes both diffusion and expansion. Fig. 3 presents a close-up view of the shrapnel density structure at \( t = 2500 \) yr, showing that, while the outer parts of the knot diffuse and mix with the expanding ejecta, its central core remains much denser. The density of the core of the clump drops down much more slowly than that of the spherically expanding ejecta. Therefore, the inhomogeneous rarefaction of the knot makes the density contrast between the core of the shrapnel and the expanding ejecta higher, and \( \chi \) rapidly increases until the shrapnel reaches the reverse shock. We computed \( \chi \) during the expansion phases, by calculating the shrapnel density, \( \rho_s \), as the average of the density in all the computational cells where the shrapnel content is \( >90 \) per cent.\(^4\) We then divided \( \rho_s \) by the ejecta density (along the \( r \)-axis) at the same distance from the origin as the shrapnel centre. Fig. 4 shows the evolution of \( \chi \) as a function of time for the \( R1/3 - CHI20 \) simulation. The figure shows that the ejecta knot reaches \( \chi > 100 \) as it approaches the reverse shock, hence our results are in agreement with those of WC02. Our model shows that a knot that was only 20 times denser than the surrounding ejecta (at the beginning of the simulations) can reach the SNR main shock without being fragmented in the intershock region and can produce protrusions that are similar to those actually observed in the Vela SNR.

\(^{4}\) These cells are closer to the centre of the knot, and are less affected by the diffusion.
Modelling of the Vela shrapnel

shrapnel is beyond the shock front and there is a significant fraction of the ejecta knot material (the shrapnel tail) that is inside the SNR shell and that is expected to emit thermal X-rays (see Section 4).

We point out that in SNRs the efficiency of thermal conduction can be significantly reduced by the presence of the magnetic field (which is not taken into account in our model). If we assume an organized ambient magnetic field, the thermal conduction is anisotropic, because the conductive coefficient in the direction perpendicular to the field lines is several orders of magnitude lower than that parallel to the field lines, which coincides with the Spitzer coefficient $\kappa(T)$. The effects of the magnetic-field-oriented thermal conduction in the interaction between shocks and dense clump have been investigated in detail in Orlando et al. (2008). Because of the high beta of the plasma, the magnetic field lines are expected to envelope the hydrodynamic fingers thus hampering the thermal conduction with the surrounding material. At the same time, the magnetic field is expected to be trapped at the top of the ejecta clumps, and this yields to an increase of the magnetic pressure and field tension which limits the growth of hydrodynamic instabilities (see O12 and Sano et al. 2012).

The basic physics of the interaction between the ejecta knots and the SNR shocks is similar to that for the interaction of planar shocks with an interstellar cloud (e.g. WC02) and it has been shown that, in this case, simulations including thermal conduction in an unmagnetized plasma and pure HD simulations are limiting cases that encompass the results obtained with different configurations of the magnetic field (Orlando et al. 2008). We can then conclude that our simulations provide the two extreme cases that bracket all the possible intermediate scenarios.

3.3 Effects of the initial conditions

We study the effects of the initial conditions on the shrapnel evolution with different simulations, as shown in Table 1. In particular, we explored two different initial positions of the shrapnel in the ejecta profile ($R_{ej} = 1/6 R_{\odot}$, $1/3 R_{\odot}$) and three different density contrasts ($\chi = 10, 20, 50$).

In agreement with WC02, we found that shrapnel formed in the inner ejecta layers (i.e. those that reach the reverse shock later) produce smaller protrusions. In particular, an ejecta knot originating at $R_{ej} = 1/6 R_{\odot}$ does not even reach the SNR shock in the time spanned by our simulations. Therefore, our model indicates that Shrapnel A–F (all protruding well beyond the Vela main shock) originated in more external layers. Left-hand panel of Fig. 7 shows the 2D cross-sections through the $(r, z)$ plane of temperature and density at the age of the Vela SNR for the $R_{ej}/6 - CHI$ simulation. In this case, the knot is well within the intershock region, even though its initial density contrast ($\chi = 50$) was higher than that of the $R_{ej}/3 - CHI$ run. However, our models of knots originating at $R_{ej} = 1/3 R_{\odot}$ clearly show that denser shrapnel produce deeper protrusions and are more stable against the fragmentation and the deceleration induced by the hydrodynamic instabilities in the intershock region (as in WC02).5 Fig. 7, right-hand panel, shows the 2D cross-sections through the $(r, z)$ plane of temperature and density at the age of the Vela SNR for the $R_{ej}/3 - CHI$ simulation. As expected, the shrapnel head is much further away from the SNR shell than in the $R_{ej}/3 - CHI$ case (shown in the right-hand panel of

5 In our runs, higher values of $\chi$ correspond to smaller values of the shrapnel cross-section (given that the shrapnel mass is fixed to $1.19 \times 10^{33}$ g in all our simulations), and this concurs in making the knot a more penetrating bullet.

Figure 6. Temporal evolution of $MX_{\text{shra}}$ (mass of the plasma in the computational cells consisting of the original shrapnel material by more than 90 per cent and having a temperature higher than $10^6$ K) for the simulations $R_{1/3} - CHI20 - TR$ (blue curves) and $R_{1/3} - CHI20$ (black curves). The dashed lines indicate the part of $MX_{\text{shra}}$ that protrudes beyond the SNR shock front.

where $\kappa(T) = 5.6 \times 10^{-7} T^{5/2}$ erg s$^{-1}$ K$^{-1}$ cm$^{-1}$ is the Spitzer coefficient and $l$ is the characteristic length of temperature variation. Therefore, the thermal conduction time-scale is

$$\tau_{\text{cond}} = \frac{7nk}{2(y - 1) \kappa(T)} \sim 2.6 \times 10^{-9} \frac{n l^2}{T^{7/2}} \text{[s].}$$

(4)

For a characteristic structure with size $l \sim 4 \times 10^{16}$ cm, particle density $n = 0.8$ cm$^{-3}$, Atwood number $A \sim 0.44$, $\Delta T \sim 2 \times 10^7$ cm/s, $T \sim 1.3 \times 10^7$ K (similar to that shown in Fig. 2), $\tau_{\text{cond}} \sim 1.4 \tau_{\text{cond}} \sim 2000$ yr. Therefore, the thermal conduction diffusive processes develop faster than the hydrodynamic instabilities and density and temperature inhomogeneities are smoothed out before they can grow.

The evolution of the position of the shrapnel head and the protrusion it produces to the remnant shock front are similar to those obtained without including thermal conduction and radiative cooling. Nevertheless, the shrapnel evolution is remarkably different from that obtained in the pure hydrodynamic (HD) simulations. In particular, as shown by the blue contours in Fig. 5, the ejecta knot is elongated along its direction of motion and rapidly assumes a cometary shape, characterized by a prominent tail which is rich in shrapnel material. After $t = 11,000$ yr, shrapnel material is present at $\sim 10$ pc away from the shrapnel head. Moreover, the shrapnel material is efficiently heated by thermal conduction with the surrounding shocked ejecta. Let $MX_{\text{shra}}$ be the mass of the plasma in the computational cells consisting of the original shrapnel material by more than 90 per cent and having a temperature higher than $10^6$ K (and therefore emitting thermal X-rays). Fig. 6 shows the evolution of $MX_{\text{shra}}$ as a function of time for the simulations $R_{1/3} - CHI20 - TR$ and $R_{1/3} - CHI20$. When thermal conduction is at work, $\sim 90$ per cent of the original shrapnel mass is heated up to X-ray emitting temperature at $t = 11,000$ yr (i.e. at the age of the Vela SNR), while if thermal conduction in inhibited, only $50$ per cent of the original mass has temperature higher than $10^6$ K. Fig. 6 also shows the amount of X-ray mass beyond the shock front. In the pure HD simulation, the hot shrapnel material is all beyond the SNR shock front. In the $R_{1/3} - CHI20 - TR$ simulation, only part of the X-ray emitting...
Fig. 2). We computed the time evolution of $\chi$ for the $R_1/3 - CHI50$ run by following the procedure described in Section 3.1. We found that, in this case, the ejecta knot reaches the reverse shock with a very high density contrast ($\chi > 1000$, see Fig. 8), thus producing a very prominent protrusion in the SNR.

Fig. 9 shows the position of the shrapnel head (in units of the shell radius $R_{\rm shell}$) as a function of time for all the simulations listed in Table 1. The black curves indicate pure hydrodynamic models, while the blue curves indicate simulations including thermal conduction and radiative cooling. The dashed/solid/thick lines indicate $\chi = 10/20/50$, respectively. The red diamonds show the projected positions of Shrapnel A–D (Aschenbach et al. 1995) and of the ejecta knots FilE and RegNE (Miceli et al. 2008).

tre with coordinates $\alpha_{2000} = 8^h36^m19.8^s$, $\delta_{2000} = -45^\circ24.5^\prime$.

Models including the effects of radiative cooling and thermal conduction (blue curves in Fig. 9) do not provide significant differences with respect to pure HD models (black curves) in terms of the shrapnel position.

By considering all the simulations with $R_e = 1/3 \ R_{\rm shell}$, we find that the position of the head of the knot, $R_h$, after $\sim 11$ kyr ranges between $\sim 1.1 \ R_{\rm shell}$ (for $\chi = 10$) and $\sim 1.4 \ R_{\rm shell}$ (for $\chi = 50$). These values are similar to those observed for Shrapnel B, C, and D.

Shrapnel A, E and F (Shrapnel E and F are not shown in Fig. 9) instead have $R_e = 1.57 \ R_{\rm shell}$, $R_{\chi 50}$ = 1.88 $R_{\rm shell}$ and $R_{\chi 20} = 1.91 \ R_{\rm shell}$, respectively. These values are much larger than those obtained in our simulations. Our results clearly suggest that these large distances from the shell can be produced by ejecta knots originating in outer ejecta layers. An alternative possibility is that the original density contrast for these shrapnel was >50. Nevertheless, Fig. 9 shows that the final position of an ejecta clump is more sensitive to its initial position and depends only weakly on $\chi$. In fact, by varying the initial position of the knot by a factor of 2, we found that its final position varies approximately by the same factor, while a variation of the initial density contrast by a factor of 5, only determines a 30 per cent variation in the final position. Therefore, it is more likely that Shrapnel A, E and F were produced at $R_e > 1/3 \ R_{\rm shell}$.

The two simulations with $R_e = 1/6 \ R_{\rm shell}$ show that the ejecta knots originating in the inner ejecta layers do not reach the forward shock, even for the highest density contrast ($\chi = 50$). The position of the head of the knot predicted by our simulations is in agreement with that observed for FilE (Miceli et al. 2008). X-ray emitting ejecta knots have been observed, in projection, inside the Vela SNR shell (e.g. RegNE and FilE; Miceli et al. 2008). However, we point out that the actual position of these ‘internal’ shrapnel can be well outside the SNR shell, and therefore the values reported in Fig. 9 might be considered as lower limits.

4 DISCUSSIONS AND CONCLUSIONS

The structure of the ejecta in a SNR contains the imprint of the metal-rich layers inside the progenitor star, and may help to
understand the processes occurring in the latest stage of stellar evolution. We performed a set of hydrodynamic simulations to study the evolution of the ejecta knots in the Vela SNR.

We found that moderately overdense clumps (initial density contrast \(\chi \sim 10\)) can produce protrusions in the SNR shell similar to those observed for the Vela shrapnel. WC02 found that only clumps that reach the reverse shock with density contrast \(\chi \gtrsim 100\) can reach the main shock front and produce significant protrusions. This criterion is fulfilled in all our simulations. In fact, the (initially) moderately overdense clump experiences diffusion in the ‘free’ expansion phase, and, while its outer parts mix with the surrounding ejecta, its central core remains much denser. This inhomogeneous rarefaction makes the density contrast between the core of the shrapnel and the expanding ejecta higher as the remnant evolves, and \(\chi\) reaches values \(\sim 100–1000\) at the interaction with the reverse shock.

In particular, a knot with initial \(\chi = 20\) and \(R_0 = 1/3 \, R_0^\text{ej}\) (simulations \(R1/3 - \text{CHI}20\) and \(R1/3 - \text{CHI}20 - \text{TR}\)) can explain the observed features associated with the Vela Shrapnel D. Fig. 10 shows the ROSAT All-Sky Survey image of the Vela Shrapnel D in the 0.1–2.4 keV energy band, compared with a synthesis of the X-ray emission in the 0.1–2.4 keV band derived from the \(R1/3 - \text{CHI}20 - \text{TR}\) simulation at 11 000 yr. The synthesized X-ray map has been obtained as in Miceli et al. (2006): we produced the 3D map of the emission measure and temperature in the Cartesian space \((x', y', z')\), where the \(y'\)-axis corresponds to the direction of the line of sight and is perpendicular to the \((r, z)\) plane. We derived the distribution \(EM(x', z')\) versus \(T(x', z')\) by considering all the contributions along the line of sight, for each \((x', z')\). We then synthesized the map of the X-ray emission using the \texttt{MEKAL} spectral code (Mewe, Gronenschild & van den Oord 1985; Mewe, Lemen & van den Oord 1986; Liedahl, Osterheld & Goldstein 1995), assuming a distance of 250 pc, and an interstellar column density \(N_H = 2 \times 10^{20} \text{ cm}^{-2}\).

Finally, we degraded the spatial resolution of the synthesized X-ray map to match the resolution of the ROSAT image and randomized the map by assuming Poisson statistics for the counts in each image bin.

Fig. 10 shows that the bright X-ray spot at the apex of the shrapnel bow shock and the enhanced X-ray luminosity at the base of the protrusion can be explained by our model as local enhancements of the plasma emission measure. The overall shape of the observed features is also reproduced by our model. Moreover, the mass of the X-ray emitting shrapnel predicted by our model is in agreement with that measured for Shrapnel D. In fact, it has been estimated that the X-ray emitting mass (considering only the bulge above the Vela SNR bow shock) is \(\sim 0.1 \, M_\odot\) (Katsuda & Tsunemi 2005), i.e. the same order of magnitude as that obtained in our simulation (see dashed curves in Fig. 6). Vela Shrapnel D is therefore consistent with being originated by an ejecta knot 20 times denser than the surrounding ejecta and initially located at \(1/3 \, R_0^\text{ej}\). As shown in Fig. 9, we found a degeneracy in the space of the initial parameters, and similar results can be obtained also by enhancing/decreasing the density contrast and decreasing/increasing the initial distance of the knot to the explosion centre. However, as explained in Section 3.3, the final position of the shrapnel is much more sensitive to its initial position in the ejecta profile. In conclusion, according to our model, the original position of Shrapnel D should not differ much from \(1/3 \, R_0^\text{ej}\).

As shown in Section 3.3, our model suggests that Shrapnel B, C and D were all originated at \(\sim 1/3\, R_0^\text{ej}\). This conclusion is in agreement with the results of X-ray data analysis that show that Shrapnel B and D have similar abundance patterns (Katsuda & Tsunemi 2005; Yamaguchi & Katsuda 2009). The fragment RegNE,
which appears inside the Vela shell, has similar abundances as Shrapnel D (Miceli et al. 2008) and its position is compatible with an origin in the same layer where Shrapnel B, C and D were generated.\footnote{In this case, its projected distance from the centre of the SNR must be much smaller than its actual distance.}

In Section 3.3, we also pointed out that it is highly unlikely that Shrapnel A originated in the same ejecta layer as Shrapnel D. Indeed, the abundance patterns observed in Shrapnel A are remarkably different from that observed in Shrapnel B and D (Katsuda & Tsunemi 2006), thus suggesting a different location of this knot in the ejecta profile. Nevertheless, the Si:O ratio is much higher in Shrapnel A than in Shrapnel D and this indicates that Shrapnel A comes from a region of the progenitor star below that of the Shrapnel D (e.g. Tsunemi & Katsuda 2006), at odds with our predictions. As explained above, an unrealistically high initial $\chi$ is required for an inner shrapnel to overcome outer knots, if we assume that the initial velocity profile of the ejecta increases linearly with their distance from the centre. A possible solution for this puzzling result is that the Si burning layer (or part of it) has been ejected with a higher initial velocity, e.g., as a collimated jet. It is noteworthy to remark that in other core-collapse SNRs the Si-rich ejecta may show a very peculiar jet–counterjet structure. The well-known case of Cas A has been studied in detail thanks to a very long Chandra observation (Hwang et al. 2004) showing a jet (with a weaker counterjet structure) composed mainly of Si-rich plasma. Laming et al. (2006) have performed X-ray spectral analysis of several knots in the jet and concluded that the origin of this interesting morphology is due to an explosive jet and it is not arising because of an interaction with a cavity or other ISM/CSM peculiar structure. Therefore, a jet origin for the Si-rich knots is sound.

Finally, we investigated the effects of thermal conduction, finding that it determines an efficient ‘evaporation’ of the ejecta knot and accelerate its mixing with the surrounding medium. Moreover, it affects the shrapnel morphology, producing the formation of a long, metal-rich tail. Enhanced metallicities have been observed in the tails of Shrapnel A, B and D and the abundance analysis performed on the X-ray spectra clearly suggests an efficient mixing of the ejecta knots with the surrounding medium (Katsuda & Tsunemi 2005, 2006; Yamaguchi & Katsuda 2009). These results are in qualitative agreement with our findings. A quantitative comparison between models and observations requires a forward modelling approach, consisting in the synthesis of the X-ray spectra from the simulations and a detailed comparison between the synthesized observables and the corresponding observations (e.g. through a spatially resolved spectral analysis, as in Miceli et al. 2006, e.g.). Moreover, it will also be important for future models to include some seed magnetic fields in the simulations to study how tangled the field becomes and what this implies for thermal conduction. These further studies are beyond the scope of this paper.

In conclusion, our hydrodynamic modelling of ejecta knots in the Vela SNR allowed us to find: (i) the observed shrapnel can be the results of moderate density inhomogeneities in the early ejecta profile; (ii) the evolution of a shrapnel in the SNR is very sensitive to its initial position and depends much less (but does depend) on the initial density contrast; (iii) thermal conduction plays an important role and explains the efficient mixing of the ejecta knots observed in X-rays.

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REFERENCES

Anderson M. C., Jones T. W., Rudnick L., Tregillus I. L., Kang H., 1994, ApJ, 421, L31
Aschenbach B., Egger R., Trumper J., 1995, Nat, 373, 587
Bocchino F., Maggio A., Scintino S., 1999, A&A, 342, 839
Cha A. N., Sembach K. R., Danks A. C., 1999, ApJ, 515, L25
Chevalier R. A., 2005, ApJ, 619, 839
Cid-Fernandes R., PLEWA T., Różycka M., FRANCO J., TERLEVICH R., TENORIO-TAGLE G., Miller W., 1996, MNRAS, 283, 419
DeLaney T. et al., 2010, ApJ, 725, 2038
Fesen R. A. et al., 2006, ApJ, 645, 283
Fryxell B. et al., 2000, ApJS, 131, 273
Hammell M. C., Fesen R. A., 2008, ApJS, 179, 195
Hwang U., Laming J. M., Badenes C., Berendse F., Blondin J., Cifelli D., DeLaney T., Dewey D., 2004, ApJ, 615, L117
Jones T. W., Kang H., Tregillis I. L., 1994, ApJ, 432, 194
Katsuda S., Tsunemi H., 2005, PASJ, 57, 621
Katsuda S., Tsunemi H., 2006, ApJ, 642, 917
Katsuda S., Kashi, H., Tsunemi H., Park S., Hwang U., Burrows D. N., Hughes J. P., Slane P. O., 2008, ApJ, 678, 297
Klein R. I., McKee C. F., Colella P., 1994, ApJ, 420, 213
LaMassa S. M., Slane P. O., de Jager O. C., 2008, ApJ, 689, L121
Laming J. M., Hwang U., Radics B., Lekli G., Takács E., 2006, ApJ, 644, 260
Liedahl D. A., Osterheld A. L., Goldstein W. H., 1995, ApJ, 438, L115
Lohner R., 1987, Comput. Methods Appl. Mech. Eng., 61, 323
Mewe R., Gronenschild E. H. B. M., 1986, Ap&AS, 62, 197
Mewe R., Lemen J. R., van den Oord G. H. J., 1984, A&AS, 65, 511
Miceli M., Reale F., Orlando S., Bocchino F., 2006, A&A, 458, 213
Miceli M., Bocchino F., Reale F., 2008, ApJ, 676, 1064
Miyata E., Tsunemi H., Aschenbach B., Mori K., 2001, ApJ, 559, L45
Orlando S., Peres G., Reale F., Bocchino F., Rosner R., Plewa T., Siegel A., 2005, A&A, 444, 505
Orlando S., Bocchino F., Reale F., Peres G., Pagano P., 2008, ApJ, 678, 274
Park S., Hughes J. P., Slane P. O., Burrows D. N., Roming P. W. A., Nousek J. A., Garmire G. P., 2004, ApJ, 602, L33
Richtmyer R. D., 1960, Commun. Pure Appl. Math., 13, 297
Sano T., Nishihara K., Matsuoka C., Inoue T., 2012, ApJ, 758, 126
Santo T., Nishihara K., Matsuoka C., Inoue T., 2012, ApJ, 758, 126
Spitzer L., 1962, Physics of Fully Ionized Gases, 2nd edn. Interscience, New York
Taylor J. H., Manchester R. N., Lyne A. G., 1993, ApJS, 88, 529
Taylor J. H., Manchester R. N., Lyne A. G., 1993, ApJS, 88, 529
Tsunemi H., Katsuda S., 2006, New Astron. Rev., 50, 521
WANG C.-Y., Chevalier R. A., 2002, ApJ, 574, 155 (WC02)
Yamaguchi H., Katsuda S., 2009, ApJ, 696, 1548

APPENDIX A: TEST ON SPATIAL RESOLUTION

As explained in Section 2.1, the spatial resolution of our simulations is reduced by a factor of 2 at $t > 2500$ yr. To check whether this resolution is sufficient to capture the basic evolution of the system, we repeated simulation R1/3 – CHI20 by maintaining the finest
level of resolution at its initial value ($1.95 \times 10^{16}$ cm, hereafter simulation $R1/3 - CHI20 - hiRES$) for the whole run. We verified that simulations $R1/3 - CHI20$ and $R1/3 - CHI20 - hiRES$ yield very similar results and all the quantities discussed in the paper (position of the shrapnel as a function of time, X-ray emitting mass of the shrapnel, etc.) do not change significantly. Fig. A1 shows the 2D cross-sections of the density through the $(r, z)$ plane obtained for simulations $R1/3 - CHI20$ and $R1/3 - CHI20 - hiRES$ at $t = 5000$ yr. This evolutionary stage is the most critical, since the system is still relatively small and the ejecta knots interact with the hydrodynamic instabilities in the intershock region. Fig. A1 clearly proves that simulation $R1/3 - CHI20$ already provides a very accurate description of the system and run $R1/3 - CHI20 - hiRES$ does not introduce any major differences.

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