Applying Constraint Handling Rules to HPSG

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June 30, 2000

Abstract

Constraint Handling Rules (CHR) have provided a realistic solution to an over-arching problem in many fields that deal with constraint logic programming: how to combine recursive functions or relations with constraints while avoiding non-termination problems. This paper focuses on some other benefits that CHR, specifically their implementation in SICStus Prolog, have provided to computational linguists working on grammar design tools. CHR rules are applied by means of a subsumption check and this check is made only when their variables are instantiated or bound. The former functionality is at best difficult to simulate using more primitive coroutining statements such as SICStus when/2, and the latter simply did not exist in any form before CHR.

For the sake of providing a case study in how these can be applied to grammar development, we consider the Attribute Logic Engine (ALE), a Prolog preprocessor for logic programming with typed feature structures, and its extension to a complete grammar development system for Head-driven Phrase Structure Grammar (HPSG), a popular constraint-based linguistic theory that uses typed feature structures. In this context, CHR can be used not only to extend the constraint language of feature structure descriptions to include relations in a declarative way, but also to provide support for constraints with complex antecedents and constraints on the co-occurrence of feature values that are necessary to interpret the type system of HPSG properly.

Constraint Handling Rules [CHR, Frühwirth and Abdennadher, 1997] have provided a realistic solution to an over-arching problem in many fields that deal with constraint logic programming: how to combine recursive functions or relations with constraints while avoiding non-termination problems. Potential applications of constraint logic programming within computational linguistics have certainly not been immune to this problem, and for them, CHR is currently the only existing tractable alternative to manually specifying a set of delay statements to avoid non-termination in a space of constraints with huge numbers of non-deterministic constraints and relational attachments that are almost invariably recursive.

This paper focuses on some other benefits that CHR, specifically its implementation in SICStus Prolog, has provided to computational linguists working on grammar design tools. CHR rules are applied through a subsumption check and this check is made only when their variables are instantiated or bound. The former functionality is at best difficult to simulate using more primitive coroutining statements such as SICStus when/2, and the latter simply did not exist in any form before CHR, to the best of this author’s knowledge.

For the sake of providing a case study in how these can be applied to grammar development, we will consider the Attribute Logic Engine (ALE) [Carpenter and Penn, 1996], a Prolog prepro-
cessor for logic programming over the logic of typed feature structures [Carpenter, 1992], and its extension to a complete grammar development system for Head-driven Phrase Structure Grammar (HPSG) [Pollard and Sag, 1987, 1994], a popular constraint-based linguistic theory that uses typed feature structures. A great many details of HPSG have changed since its inception and still more are yet to be agreed upon, so the presentation here is by necessity a tremendous simplification. Nevertheless, it is hoped that this paper will stimulate a discussion of what limit CHR permits us to extend the state of the art in grammar development to, and what future developments on the part of implementors of logic programming languages such as Prolog would be most beneficial in order to push that limit even further.

The next three sections give a very brief introduction to the view of human languages that HPSG takes, how typed feature structures fit into that view, and what the basic constraint-solving problem is that grammar developers are faced with. Section 4 then shows how to compile these general constraints into more atomic ones and where CHR fills in the gap in providing an elegant implementation of this in Prolog. Section 5 illustrates another kind of constraint that must be dealt with internally by HPSG grammar development systems, and how CHR provides the unique ability to do that efficiently.

Finally, Section 6 points to a few issues that still remain to be resolved relative to what Prolog with its CLP extensions is currently able to provide, namely a more efficient implementation of attributed variables and a means for universal quantification of constraints.

1 Head-driven Phrase Structure Grammar

HPSG is a theory that seeks to predict the grammaticality, or syntactic well-formedness, of utterances in any human language. It is sometimes called a realist theory of language, as opposed to a mentalist theory of language, because grammatical utterances from human languages are taken to be actual entities that exist in the world. As such, these entities constitute a universe of objects for a model that we seek to describe using HPSG. The principal role of a grammar development system in this context is to provide the means to state theories of human language formally, and then to ask whether the formal representation of a candidate utterance with a particular phonological realization, i.e., one comprised of a particular string of words, has a non-empty denotation in this model.

By convention, the theory itself is stated using the formal language of the logic of typed feature structures. Typed feature structures are a semantically typed kind of record, which is a very convenient representation for linguistic purposes because the combination of typing with named attributes allows for a very terse description language that can easily make reference to a sparse amount of information in what are usually extremely large structures/records. There are actually several variations of that language in circulation, e.g., Carpenter, 1992, King, 1989, Smolka, 1988, which are more or less well-suited to the purposes of HPSG, or, perhaps more historically accurate, to the rules of which linguists working with HPSG more or less elected to adhere. The language that the seminal work on HPSG of Pollard and Sag [1994] actually uses was finally formalized in its own right by Richter [2000], Richter et al. [1999]. The bad news is that satisfiability in this language is not even compact. The good news is that no one particularly seems to care about the bad news. This is due to the fact that: (1) most of the work performed by linguists in HPSG is not actually formalized in this language, thus creating a gap between theory and practice that must be bridged in the course of formalization in a grammar.
development system anyway; and (2) most grammar development systems have, for years, elected
to follow a much more conservative route inspired by work in constraint logic programming, in
which a core constraint language for describing typed feature structures has been extended
with a relational definite clause language [H¨ohfeld and Smolka, 1988] for conveniently stating
the “constraints,” or as they are called in linguistics, principles, that define grammaticality in
human language. The core constraint language that will be assumed here is essentially the one
defined by Carpenter [1992], with an eye towards the view of feature structures in HPSG taken
by King [1999].

2 Typed Feature Structures and their Descriptions

Each typed feature structure is a tuple \( \langle Q, \theta, \delta \rangle \), where \( Q \) is a set of nodes (corresponding to
substructures of feature structures), \( \theta \) is a total typing function that maps nodes to a fixed
finite meet semi-lattice of types, \( \text{Type} \), and \( \delta \) is a partial feature value function that maps pairs
consisting of a feature, drawn from a finite set, \( \text{Feat} \), and a node in \( Q \) to nodes in \( Q \). Typed
feature structures are conventionally depicted as records, such as:

\[
\begin{array}{c}
\text{throwing} \\
\text{THROWER} \\
\text{THROWN} \\
\text{index} \\
\text{PERSON} \\
\text{NUMBER} \\
\text{masculine} \\
\text{gender} \\
\text{third} \\
\text{singular} \\
\end{array}
\]

In this example, there is a total of eight nodes, one of type \text{throwing}, two of type \text{index}, two
of type \text{third}, and one each of type \text{singular}, \text{masculine} and \text{neuter}. Note that the numeric
tag (called a \text{re-entrancy}) indicates that the two number features have extensionally the same
value, which is of type \text{singular}, whereas the two person features have different feature structure
values, i.e., different nodes, that happen to be of the same type, \text{third}. Typed feature logics are
normally intensionally typed, so this identity of type does not imply an extensional identity of
feature values. We can refer to substructures of feature structures along paths, provided that
the values of each feature on the path exist. The THROWER:GENDER value of this example is of
type \text{masculine}.

The core constraint language itself is a description logic for talking about feature structures
relative to the finite meet semi-lattice of types, \( \text{Type} \), a fixed finite set of features, \( \text{Feat} \), and a
countable set of variables, \( \text{Var} \):

The description language, \( \Phi \), is the least set of descriptions that contains:

- \( v, v \in \text{Var} \),
- \( \tau, \tau \in \text{Type} \),
- \( f : \phi, f \in \text{Feat}, \phi \in \Phi \),
- \( \phi_1 \land \phi_2, \phi_1, \phi_2 \in \Phi \), and
• $\phi_1 \lor \phi_2, \phi_1, \phi_2 \in \Phi$.

A nice property of this language is that every non-disjunctive description with a non-empty denotation has a unique most general feature structure in its denotation. This is called its *most general satisfier*. Of course, this is not the same kind of denotation as the one that connects our theory to language itself — there are two levels of abstraction at work. Descriptions denote sets of feature structures, and feature structures denote sets of utterances in the world.

A given set of types and features is also typically augmented with a set of *appropriateness conditions* that mediate their occurrence, following King [1989] and Carpenter [1992]. Appropriateness conditions stipulate, for every type, a finite set of features that can and must have values in feature structures of that type. This effectively forces feature structures to be finite-branching terms with named attributes, although the introduction of new features combined with subtyping means that the arities of these terms are not completely fixed. Appropriateness conditions also usually restrict the value that appropriate features can take by specifying a type that must be a supertype of the value’s type.

In the formulation of Carpenter [1992], appropriateness must also guarantee that there is a unique most general type for which a given feature is appropriate. This is called *unique feature introduction*, and for feature $F$, its introducing type is called $\text{Intro}(F)$. Until recently, it was generally believed that Prolog systems that work with typed feature structures must meta-interpret unification and SLD resolution over them. As shown by Penn [2000], when unique feature introduction is assumed, every statically typable set of appropriateness conditions admits a Prolog term encoding of its typed feature structures, thus reducing feature structure unification to Prolog unification in the underlying Warren abstract machine. When it is not assumed, furthermore, unique feature introduction can be added automatically in polynomial time while preserving meet-semi-latticehood. This result opens the door to using pieces of Prolog implementations’ enhanced functionality, including CHR, that would have been prohibitively less elegant if even only unification needed to be meta-interpreted.

### 3 The Language of Principles

Principles can be divided into two classes: those that apply to all languages, and those that only apply to specific languages. The lexicon itself can be regarded as a very disjunctive principle — language-specific, of course — associating each word to a specific syntactic and semantic representation. This paper will not say much more about the lexicon.

In HPSG, and, in fact, in nearly every constraint-based theory of grammar, all principles, regardless of class, take the form of a statement, “for all terms/feature structures, statement $\pi$ holds.” In contrast to most work in constraint logic programming, every constraint is thus implicitly universally quantified over typed feature structures, and thus not explicitly posted to a store. In practice, nearly every principle’s $\pi$ takes the form of an implication, and for most complex principles, $\pi$ makes reference to instances of relations. The approach taken here is that all $\pi$ are of the form:

$$\alpha \implies (\gamma \land \rho)$$

where $\alpha$ and $\gamma$ are descriptions from the core constraint language and $\rho$ is drawn from a definite clause language of relations, whose arguments are also descriptions from the core constraint
language. Typically, these arguments include variables that are also used in \( \gamma \), so that variables take scope over the entire consequent.

This form is somewhat of an idealization itself. Linguists often formulate principles in which variables are shared between \( \alpha \) and the consequent, with the intention that \( \alpha \Rightarrow (\gamma \land \rho) \) should actually be \( \alpha \Rightarrow (\alpha \land \gamma \land \rho) \). Sometimes, they also use relations in \( \alpha \) rather than just descriptions from the core language, for the interpretation of which negation by failure or some other extra convention must be used. These will be ignored in the rest of this paper, although the method described below for dealing with this form of principle can be extended in several ways to attempt to handle these more complicated antecedents as well.

The presumed form of these principles is not new. The ALE system permits the same form, but where \( \alpha \) can only be a type description, \( \tau \). The ConTroll system [Goetz and Meurers, 1997] permits essentially the same form, but interprets the implications classically, which creates a very large search space with severe non-termination problems because of the presence of potentially recursively defined relations in \( \rho \). ConTroll attempted to remedy this problem by providing a language of delays, similar to coroutining predicates in Prolog but with the extra implicit universal quantification built in. Repeated attempts at large-scale development with this method proved unpromising, as finding the right set of delays actually proved to be more work than simply using a more traditional deductive strategy such as SLD resolution or definite clause grammars. Such delays are also non-modular relative to changes in other parts of the grammar, which is of particular concern since grammar development is largely characterized by a large number of small incremental changes.

By contrast, the approach taken here is to allow for arbitrary \( \alpha \) but to interpret the implications using subsumption by \( \alpha \), i.e., for every feature structure (the implicit universal quantification is still there), either the consequent holds, or the feature structure is not subsumed by the most general satisfier of \( \alpha \). This decision draws its inspiration from three sources. First, ALE used the same interpretation, although somewhat more controversially given that \( \alpha \) could only be a type. Second, it is widely believed in the linguistics community [Hinrichs and Nakazawa, 1996] that lexical rules, closure conditions on the well-formedness of a lexicon, are intended to apply by subsumption. They also take the form of implications, as “if \( \lambda_1 \) is part of the lexicon, then so is \( \lambda_2 \),” in which \( \lambda_1 \) and \( \lambda_2 \) are specified using descriptions with or without some extra level of default reasoning. One can, in fact, also find many instances of principles in theoretical linguistics literature in which a subsumption-based interpretation is the intended one. The third source is the approach to CHR in its SICStus Prolog implementation, in which the head of a rule is matched using a subsumption check. The fact that linguistic theory, conventional grammar development practice and the CHR package agree on this point is very significant, and is exploited by our implementation.

The subsumption-based approach is sound with respect to the classical interpretation of implication for those cases of principles when the classical interpretation really is the correct one. For completeness, other resolution methods must be used. These are available from true constraint logic programming, which as of yet is surprisingly absent from linguistic research on constraint-based grammar. CHR can provide those additional resolution methods as well, of course.
4 Principle Decomposition

Under these assumptions, every linguistic principle can be decomposed into a series of more atomic constraints that can easily be implemented. It should first be noted that the existence of a CHR package for Prolog terms easily admits a CHR package for typed feature structures, where feature descriptions in the arguments of constraints are translated to the term encodings of their most general satisfiers. The result can then be compiled by the underlying Prolog CHR library’s compiler. This immediately provides grammar developers with an alternative to providing explicit delay statements that has proven to be far more robust and tractable for large-scale grammar development. The rest of this section concerns the compilation of the universally quantified principles themselves.

4.1 Finding a Trigger

Let \( \text{trigger}(\alpha) \) be defined such that:

- \( \text{trigger}(v) = \bot \),
- \( \text{trigger}(\tau) = \tau \),
- \( \text{trigger}(F : \phi) = \text{Intro}(F) \),
- \( \text{trigger}(\phi_1 \land \phi_2) = \text{trigger}(\phi_1) \sqcup \text{trigger}(\phi_2) \), and
- \( \text{trigger}(\phi_1 \lor \phi_2) = \text{trigger}(\phi_1) \sqcap \text{trigger}(\phi_2) \),

where \( \bot \) is the most general type in \( \text{Type} \), and \( \sqcup \) and \( \sqcap \) are join (unification) and meet (generalization) in \( \text{Type} \). \( \bot \) and meet exist given the assumption that \( \text{Type} \) is a meet semi-lattice. From that same assumption, join exists between any pair of consistent types.

If we had a predicate, \( \text{fswhen}(V=\text{Desc}, \text{Goal}) \), available such that we could delay \( \text{Goal} \) until \( V \) was subsumed by the most general satisfier of \( \text{Desc} \), then all principles:

\[ \alpha \implies (\gamma \land \rho) \]

could be converted into:

\[ \text{trigger}(\alpha) \implies v \land \text{fswhen}((v = \alpha), ((v = \gamma) \land \rho)) \]

This form (with the exception of \( \text{fswhen}/2 \)) is the form already implemented by ALE, including its implicit universal quantification. This typically involves compiling unifications of feature structures into unifications of their term encodings plus a type check to see whether one or more principle consequents need to be applied. The conditions under which that check must be made can, of course, be statically optimized to a bare minimum, but in the worst case, it significantly compromises the speed of what would otherwise be a simple Prolog-level unification. This point is discussed further in Section 6.

As a running example, we can consider a principle from the HPSG grammar for German under development at the University of Tübingen:

\[
\text{synsem:loc:cat:(head:verb, marking:fin)}
\implies \text{synsem:loc:cat:head:vform:bse}.
\]
This is called the Finiteness Marking Principle. The description to the left of the implication selects feature structures whose substructure on the path SYNSEM:LOC:CAT satisfy two requirements: that their HEAD value is of the type verb and that their MARKING value is of the type fin. The principle says that every feature structure that satisfies that description must also have a SYNSEM:LOC:CAT:HEAD:VFORM value of type bse. The problem is that feature structures may not have substructures that are specific enough to determine whether this constraint holds or not. This can happen when a type subsumes several more specific subtypes of which only one meets the requirements set forth by the constraint, for example. So we must wait until it is known whether the antecedent is true or false before applying the consequent. If we reach a deadlock, where several constraints are suspended on their antecedents, then we must use another resolution method to begin testing more specific extensions of the feature structure in turn.

To find the trigger in this example, we can observe that the antecedent is a feature value description (F:φ), so the trigger is Intro(SYNSEM), the unique introducer of the SYNSEM feature, which happens to be the type sign. We can then transform this constraint to:

\[
\text{sign cons } X \\
\text{goal fswhen((X=synsem:loc:cat:(head:verb, marking:fin)),} \\
\text{ (X=synsem:loc:cat:head:vform:bse)).}
\]

The cons and goal operators are defined by ALE, and used to separate the type antecedent from the description component of the consequent (in this case, just the variable, X), and the description component of the consequent from its relational attachment. We know that any feature structure subsumed by the original antecedent will also be subsumed by the most general feature structure of type sign, because sign introduces SYNSEM.

### 4.2 Reducing Complex Conditionals

The next step is to decompose fswhen/2 itself. For simplicity, it can be assumed that its first argument is actually drawn from a more general conditional language, including those of the form \( V = Desc \) and closure under conjunction and disjunction. Also for simplicity, it is assumed that the variables of each \( Desc_i \) are distinct.

Such a complex conditional can easily be converted into a normal form in which for each atomic conditional, \( V_i = Desc_i \), \( Desc_i \) is non-disjunctive. Just as with the principles themselves, we can begin by isolating types and assuming that we have a predicate typewhen(Type,V,Goal) that delays Goal until \( V \) is of type Type. We can then convert all of the other conditionals to this by converting fswhen(C,Goal) to Conv, i.e., reduce(C,Goal,Conv), where reduce/3 is defined such that:

\[
\begin{align*}
\text{reduce}((VD1,VD2),Goal,Conv) & : - \quad \% \text{fswhen}((VD1,VD2),Goal) \text{ iff} \\
\text{reduce}(VD2,Goal,Goal2), & \quad \% \text{fswhen}(VD1,\text{fswhen}(VD2,Goal)) \\
\text{reduce}(VD1,Goal2,Conv). & \\
\text{reduce}((VD1;VD2),Goal,(Conv1,Conv2)) & : - \\
\text{reduce}(VD1,(\text{prolog}(\text{Trigger} = 0) \rightarrow \text{Goal} ; \text{true}),\text{Conv1}), \\
\text{reduce}(VD2,(\text{prolog}(\text{Trigger} = 1) \rightarrow \text{Goal} ; \text{true}),\text{Conv2}).
\end{align*}
\]
reduce(V=Desc,Goal,Conv) :-
    vars_of(Desc,Vars),
    desc_reduce(Desc,V,Goal,Vars,_,Conv).

and desc_reduce/6 is defined such that desc_reduce(Desc,V,Goal,Vars,VarsRest,Conv) holds if and only if fswhen(V=Desc,Goal) reduces to Conv and Vars-VarsRest is the collection of all Vars that occur in Desc:

desc_reduce(X,V,Goal,Vars,VarsRest,Conv) :-
    var(X),
    !,( select(Vars,X,VarsRest) -> Conv = (V = X,call(Goal))
        % if first occurrence of X, bind to V
        ; Conv = when(?=(V,X),((V==X) -> call(Goal) ; true)),
          VarsRest = Vars
        % otherwise, wait until V==X )
).

desc_reduce(F:Desc,V,Goal,Vars,VarsRest,typewhen(IntroType,V,(farg(F,V,FVal),
    call(DescConv)))) :-
    intro(F,IntroType),
    desc_reduce(Desc,FVal,Goal,Vars,VarsRest,DescConv).

desc_reduce(T,V,Goal,Vars,Vars,Conv) :-
    type(T),
    !, Conv = typewhen(T,V,Goal).

desc_reduce((Desc1,Desc2),V,Goal,Vars,VarsRest,Conv2) :-
    desc_reduce(Desc1,V,Goal,Vars,VarsMid,Conv1),
    desc_reduce(Desc2,V,Conv1,VarsMid,VarsRest,Conv2).

Here, the prolog/1 goals are inserted without modification by a compiler, as goals in that position are normally interpreted to be relations over feature structure descriptions. The Prolog convention of comma for AND and semi-colon for OR is also used in these definitions. In the disjunctive case of reduce/3, the binding of the variable Trigger is necessary to ensure that Goal is only resolved once in case the goals for both conditionals eventually unsuspend. In the variable case, desc_reduce/6 simply binds the feature structure in question when it first encounters a variable, but subsequent occurrences of that variable create a suspension that compiles directly down to Prolog when/2, checking for identity with the previous occurrences. Notice also that Intro(F), here called IntroType, can be used as the type to delay on in the case of a feature value description. farg(F,V,FVal) binds FVal to the argument position of V that corresponds to the feature F in the term encoding of that feature structure once V has been instantiated to a type for which F is appropriate.

In the running example, we must convert the large fswhen/2 relational attachment to simpler typewhen/2 goals. The second clause of the relation, desc_reduce/6 tells us that this can be achieved by successively waiting for the types that introduce each of the features, SYNSEM, LOC, CAT. Those types are sign, syntax_semantics and local, respectively:
In practice, a great deal of static analysis is possible to reduce the complexity of the resulting relational goals. In this case, static analysis of the type system tells us that since `sign` is the trigger type, `syntax_semantics` is the least appropriate type of a `synsem` value, and `local` is the least appropriate type of a `loc` value, all three of these `typewhen/2` calls can be eliminated:

```
sign cons X goal (farg(synsem,X,SynVal),
    farg(loc,SynVal,LocVal),
    farg(cat,LocVal,CatVal),
    fswhen((CatVal=(head:verb, marking:fin)),
        (X=synsem:loc:cat:head:vform:bse))).
```

The description that `CatVal` is suspended on is a conjunctive description, so the last clause of `desc_reduce/6` tells us that we should successively suspend on each conjunct. The type that introduces both `head` and `marking` is `category`.

```
sign cons X
    goal (farg(synsem,X,SynVal),
        farg(loc,SynVal,LocVal),
        farg(cat,LocVal,CatVal),
        typewhen(category,CatVal,(farg(head,CatVal,HdVal),
            typewhen(verb,HdVal,
                typewhen(category,CatVal,(farg(markings,CatVal,MkVal),
                    typewhen(fin,MkVal,(X=synsem:loc:cat:head:vform:bse)))))
            ))
        )).
```

Since `category` is the least appropriate type of a `cat` value, static analysis again allows us to simplify the code:

```
sign cons X
    goal (farg(synsem,X,SynVal),
        farg(loc,SynVal,LocVal),
        farg(cat,LocVal,CatVal),
        farg(head,CatVal,HdVal),
        typewhen(verb,HdVal,
            (farg(markings,CatVal,MkVal),
                typewhen(fin,MkVal,(X=synsem:loc:cat:head:vform:bse))
            )
        )).
```

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4.3 Compiling Delays on Types

Delaying until a feature structure becomes at least as specific as a certain type is not so easy because of appropriateness conditions. The term encoding of a feature structure may actually reflect the type in the conditional before all of its values have been combined to create a well-formed feature structure due to the check that must be performed to enforce constraints. CHR allows one very simply to suspend until subsumption by an entire term is achieved. We define a CHR constraint typewhen/3, such that for each Type, we add a rule:

\[
\text{typewhen}(\text{Type}, \text{MGSat}, \text{Goal}) \iff \text{call}(\text{Goal}).
\]

where MGSat is the most general satisfier of Type. This constraint, when posted by the calls in \text{desc\_reduce/6} above, will wait until the variable in question is bound to something at least as specific as MGSat, which is a term encoding for which all appropriateness conditions are satisfied. Type sits in the first argument position in order to index the constraint into the correct rule more quickly.

In the running example, the term encoding of the most general satisfier of \text{sign} is:

\[
'\text{sign}'(\_,\_,'\text{mod\_syncsem}'(\text{syntax\_semantics},\_,\_),\_).
\]

The first three argument positions correspond to the three features that are appropriate to \text{sign}, the first two of which have not been mentioned here and, again by static analysis, do not need to be instantiated. The third, however, is the SYNSEM value, and the subterm in that position is the most general satisfier of the type, \text{syntax\_semantics}. The CHR compiler will create term subsumption code that causes the rule handler to wait for this feature value to be instantiated to at least this subterm, and thus satisfy the appropriateness conditions of \text{sign}. The last argument position is always an anonymous variable and preserves the intensionality of the logic. The \text{typewhen/2} clause for \text{syntax\_semantics} is thus:

\[
\text{typewhen}(\text{sign},
'\text{sign}'(\_,\_,'\text{mod\_syncsem}'(\text{syntax\_semantics},\_,\_),\_),\_), \text{Goal})
\iff \text{call}(\text{Goal}).
\]

This, of course, only uses a small part of CHR’s functionality, but it has proven to be a vital part for combining constraint resolution, coroutining, appropriateness and logic programming in the logic of typed feature structures. It is actually possible to use \text{when/2} directly to achieve the same effect, but in principle, CHR should be more efficient, because it could identify at the abstract machine level when subsumption fails, thus eliminating the constraint from the store, as soon as possible. Finding the right order in which to check the various components of a term encoding directly with \text{when/2} is not at all trivial. This point is discussed further in Section 5.

5 Subtype Covering Constraints

Another use of CHR as a very sophisticated suspension tool arises with the enforcement of a different kind of internal constraint within feature-structure-based grammar development systems. The logic of typed feature structures is a logic with subtyping, and this ordering among types induces an ordering among feature structures, called subsumption. Our view of language, however, is one of utterances that are maximally informative, and therefore discretely ordered.
As a result, what we actually care about determining in the context of grammar development is whether there is a maximally informative feature structure for a given utterance with a non-empty denotation in our realist model of language. Maximal feature structures are those in which every node is assigned a maximally specific type, and every pair of nodes with identical types is either re-entrant or explicitly inequated. Non-maximally-specific types can simply be interpreted as a short-hand for sets of their maximally specific subtypes, and non-maximal feature structures can thus be viewed as a very compact kind of representation for disjunctions of maximal feature structures.

Because of appropriateness and re-entrancies, not every feature structure has a maximal extension. Suppose type $a$ has two appropriate features, $f$ and $g$, both of whose values are restricted to the type polarity, which has maximal subtypes $+$ and $−$. $a$ could have exactly two subtypes, $b$ and $c$, with appropriateness conditions such that $b$ must have an $f$ value of $+$ and a $g$ value of $−$, and $c$ must have an $f$ value of $−$ and a $g$ value of $+$. In this case, the non-maximal feature structure:

$$
\begin{bmatrix}
  a & f \\
  G & bool \\
  \end{bmatrix}
$$

has no maximal extension because $+$ and $−$ are inconsistent. Situations such as these do occasionally arise in the realm of linguistic knowledge representation, and a grammar development system based on feature structures must detect them early in order to fail as soon as possible.

These can be implemented in ALE by adding relational attachments to ALE’s type-antecedent universal constraints that will suspend a goal on candidate feature structures with types such as $a$ that could have this problem (called deranged types). The suspended goal unblocks whenever the deranged type or the type of one of its appropriate features’ values is updated to a more specific subtype, and checks the types of the appropriate features’ values. CHR’s ability not only to suspend, but to suspend until a particular variable is instantiated or even bound to another variable is the powerful kind of mechanism required to check these constraints efficiently, i.e., only when necessary. Re-entrancies in a term encoding may only show up as the binding of two uninstantiated variables, and re-entrancies are an important case where these constraints need to be checked.

We can create a constraint, `subtype_cover/2`, whose first argument is a deranged type. For each such type, we can add three kinds of rules. The first retrieves the current type of a feature structure from its term encoding and compares it to a deranged type that it used to have.

```prolog
subtype_cover(Type,FS) <=>
  true & (type_index(FS,FSType),FSType \== Type) \\
  | true.
```

In the case of our example with $a$, $b$ and $c$, $a$ is deranged, so the following constraint handling rule is generated:

```prolog
subtype_cover(a,FS) <=>
  true & (type_index(FS,FSType),FSType \== a) \\
  | true.
```

1An inequation is a negative constraint that prohibits re-entrancies, much as in Prolog II. Their implementation is not discussed in detail here, but they can essentially be reduced to an underlying Prolog’s `dif/2` statement using the term encoding mentioned above.
If a feature structure of type $a$ is refined to be a well-formed feature structure of type $b$, then it is no longer in danger (unification over the term encoding itself fails on appropriateness failures, i.e., non-empty denotations, in such a case). In fact, no maximally specific type can be deranged. If the type has changed, then if it is still deranged, it is the responsibility of the rules for the new deranged type to check it.

The second kind of rule compares a feature structure’s appropriate feature values to a product of types that belong to one of the deranged type’s “safe” subtypes (such as its maximally specific subtypes). If this product subsumes the types of the feature structure’s current values, then it is out of danger. So for each such product, there is one rule of the form:

$$\text{subtype}\_\text{cover}(\text{Type}, \text{AppropFeatProduct}) \iff \text{true}.$$  

In the case of $a$, the following rules are generated:

$$\text{subtype}\_\text{cover}(a,'$a'(''$\text{polarity}'(+,_),'$\text{polarity}'(-,_),_)) \iff \text{true}.$$  

$$\text{subtype}\_\text{cover}(a,'$a'(''$\text{polarity}'(-,_),'$\text{polarity}'(+,_),_)) \iff \text{true}.$$  

The first rule contains a term encoding of the feature structure:

$$\begin{bmatrix}
  a \\
  F \\
  G \\
\end{bmatrix}$$

Its feature values’ types correspond to the appropriateness conditions for $b$. The second rule’s feature values’ types correspond to the appropriateness conditions for $c$. In either case, if a feature structure of type $a$ has these, then it is guaranteed to have a maximally specific extension and thus denote in the language we are modeling.

Finally, it could be that the feature structure already has no maximal extensions, or only one maximal extension. In the former case, we should fail, and in the latter case, we should extend the feature structure since that is the only possible extension it can have. The following rule uses a guard to count how many extensions are still consistent with the current feature structure: 0, 1 or more than 1. If there is more than 1, it fails, resuspending the constraint — we may still need to check later because it could lose consistency with one of those extensions. If it has 0 or 1, the guard succeeds and the body of the rule fails or extends the feature structure through unification as appropriate.

$$\text{subtype}\_\text{cover}(\text{Type}, \text{FS}) \iff \text{true & stc}\_\text{unify}\_\text{test}(\text{Type}, \text{FS}, N)$$

$$| ( N == 0 \rightarrow \text{fail}$$

$$; \% N == 1$$

$$\text{stc}\_\text{unify}\_\text{product}(\text{Type}, \text{FS}))$$

6 Further Desiderata

There are two significant shortcomings to the view of logic programming with typed feature structures presented here. The first is that feature structure unification, by far the most common
operation performed by a parser or generator based on this logic, cannot always be reduced to Prolog unification. The reason, as mentioned earlier, is that certain checks must be made in order to detect whether to apply the consequent of a “universal constraint,” a constraint that applies to literally every typed feature structure, although restrictions such as limiting the antecedent to a type and applying constraint consequences under subsumption ameliorate the cost of that task. The view of constraints in both \texttt{when/2} and CHR is that a constraint is posted relative to one or more terms and only then is its satisfaction tracked by the underlying abstract machine. What grammar developers (more specifically, people who write grammar development systems) need right now is the ability to state that a constraint universally applies, and apply that constraint to terms / feature structures efficiently at the abstract machine level. This is the only level at which it will not be necessary to disrupt term unification as ALE currently must.

The second shortcoming is the efficiency of the current CHR implementation in SICStus Prolog. This relies crucially on an attributed variables package that is rather inefficient. That inefficiency is what in fact prevents grammar developers working with feature structures from reducing those feature structures directly to attributed variables, which are at least cosmetically quite similar. This is in part due to the fact that there is no notion of appropriateness nor a strong enough notion of typing to support appropriateness, and thus encode typed feature structures as efficiently as a term encoding currently can. Simply looking at its application within CHR, however, even there, the number of allowable constraints in a handler does not scale up well, and even with a small number of constraints, delaying works far too slowly. As mentioned earlier, one can implement \texttt{typewhen/2} directly in terms of \texttt{when/2} at the cost of possibly having an overwhelming number of residual suspensions due to an unfortunate ordering of atomic suspensions that collectively implement delaying on subsumption by an entire term. Even with this large number of residues, our experiments with a large HPSG grammar for German show that a direct implementation in terms of \texttt{when/2} in SICStus Prolog is faster than using SICStus’s CHR library by a factor of 60 or more on our test suites. In principle, CHR should be much faster. Currently, the SICStus CHR compiler simply partially evaluates the necessary run-time subsumption checks, where possible, at the Prolog level.

7 Conclusion

The compilation of two kinds of constraints was proposed relative to a preprocessor for a logic programming language that term-encodes typed feature structures for a very transparent treatment of unification and constraint logic programming with feature structures within Prolog. CHR has essentially retired the problem of how best to handle the delaying of constraints within grammar development systems, although there remain a few bottlenecks to efficiency such as the universal quantification implicit to linguistic constraints and in the SICStus Prolog implementation, the underlying dependence of the CHR library on the current implementation of attributed variables.

The extension of ALE described here, called TRALE, was developed at the the University of Tübingen in parallel to a grammar of an extensive fragment of German, both of which will be made publicly available at the end of the year 2000 as deliverables of the Sonderforschungsbereich 340.
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