Statistical Study of GOES X-Ray Quasi-periodic Pulsations in Solar Flares

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Received 2020 March 30; revised 2020 April 20; accepted 2020 April 23; published 2020 May 26

Abstract

Small-amplitude quasi-periodic pulsations (QPPs) detected in soft X-ray emission are commonplace in many flares. To date, the underpinning processes resulting in the QPPs are unknown. In this paper, we attempt to constrain the prevalence of stationary QPPs in the largest statistical study to date, including a study of the relationship of QPP periods to the properties of the flaring active region, flare ribbons, and coronal mass ejection (CME) affiliation. We build upon the work of Inglis et al. and use a model comparison test to search for significant power in the Fourier spectra of lightcurves of the GOES 1–8 Å channel. We analyze all X-, M- and C-class flares of the past solar cycle, a total of 5519 flares, and search for periodicity in the 6–300 s timescale range. Approximately 46% of X-class, 29% of M-class, and 7% of C-class flares show evidence of stationary QPPs, with periods that follow a log-normal distribution peaked at 20 s. The QPP periods were found to be independent of flare magnitude; however, a positive correlation was found between QPP period and flare duration. No dependence of the QPP periods on the global active region properties was identified. A positive correlation was found between QPPs and ribbon properties, including unsigned magnetic flux, ribbon area, and ribbon separation distance. We found that both flares with and without an associated CME can host QPPs. Furthermore, we demonstrate that for X- and M-class flares, decay-phase QPPs have statistically longer periods than impulsive-phase QPPs.

Unified Astronomy Thesaurus concepts: Solar flares (1496); Solar x-ray flares (1816); Solar oscillations (1515); Solar coronal mass ejections (310)

1. Introduction

Quasi-periodic pulsations (QPPs) in solar flaring emission have been observed over the past several decades and have been widely discussed in the literature (see Nakariakov & Melnikov 2009; Van Doorsselaere et al. 2016, for recent comprehensive reviews). While there is not a strict definition for QPPs, the term is often used to describe variations of flux as a function of time that includes a characteristic timescale ranging from seconds to several minutes. The presence of QPPs in flaring lightcurves was first reported in early hard X-ray bremsstrahlung and microwave gyrosynchrotron emissions associated with flare-accelerated electrons (e.g., Parks & Winckler 1969; Chiu 1970). Indeed, the most pronounced QPPs are often observed in these wave bands during the impulsive phase of flares (e.g., Fleishman et al. 2008; Kupriyanova et al. 2010; Inglis & Dennis 2012; Zimovets et al. 2018). In recent years, however, studies have provided evidence of QPPs across a wide range of wavelengths from decimetric radio (e.g., Kupriyanova et al. 2016; Carley et al. 2019), soft X-ray and EUV (e.g., Dolla et al. 2012; Dominique et al. 2018), Lyα (Milligan et al. 2017), and even γ-rays (Nakariakov et al. 2010; Li et al. 2020), essentially encompassing all aspects of the flaring processes. It is also now clear that QPPs can occur in the decay phase of solar flares (Hayes et al. 2016), extending long after the impulsive energy release in some cases (Dennis et al. 2017; Hayes et al. 2019). There is growing evidence that the QPP phenomenon is an intrinsic feature of flaring emission (Simões et al. 2015), and likewise, well-pronounced QPPs have been observed in stellar flare lightcurves (e.g., Pugh et al. 2016) with similar properties and scalings to solar QPPs, suggesting common physical processes (Cho et al. 2016). Moreover, X-ray QPPs have have also been found to drive quasi-periodic electron density variations in Earth’s lower ionosphere (Hayes et al. 2017).

Despite the growing interest and the large number of QPP observations, the true nature of the phenomenon and the underpinning mechanism(s) remain unclear. As detailed in a recent review by McLaughlin et al. (2018), the proposed theories to explain QPPs can be categorized into oscillatory and self-oscillatory processes according to the nature of the underlying physical mechanism. In the oscillatory category, QPPs are described as a result of periodic motions about an equilibrium, such as magnetohydrodynamics (MHD) oscillations and waves in the coronal flare site (e.g., Nakariakov et al. 2006; Nakariakov & Melnikov 2009; Nakariakov & Zimovets 2011). In the self-oscillatory category, it is suggested that QPPs are an intrinsic property of the flare energy release process that has some associated timescale, such as periodic or “bursty” regimes of magnetic reconnection (e.g., McLaughlin et al. 2012; Guidoni et al. 2016; Thurgood et al. 2017). Observations to date have not been able to distinguish between these mechanisms, and it is likely that several nonexclusive mechanisms play a role. The requirement for flare models to reproduce observed QPP timescales is an important constraint. Once the mechanism(s) is (are) determined, QPPs hold the promise of providing a unique diagnostic tool for the physical processes responsible for flare energy release.

Most investigations of QPPs have focused on case studies of well-observed large solar flares (e.g., Kolotkov et al. 2018; Hayes et al. 2019). This is motivated by both the excellent statistics available for resolving flux variations and the fact that associated nonthermal emission is easier to detect in large events. Nonetheless, the identification of QPPs in smaller flares (e.g., Kumar et al. 2017) and even microflares (Nakariakov et al. 2018) has been reported. It is still unclear, however,
whether larger solar flares are more likely to produce QPPs and what conditions are necessary for the production of QPPs.

While single-event focused research is important to understand the detailed physical processes that result in flaring QPPs, large-scale statistical studies are also required to examine the general properties of QPPs such as prevalence and characteristic timescales. Instruments such as the GOES X-ray Sensor (XRS) and PROBA2/LYRA allow for such statistical studies in which fine-structure soft X-ray QPPs can be identified, often in the detrended or time-derivative lightcurves. Recent work has employed the use of such observations to study QPPs in a statistical manner, typically focusing on large X- and M-class flares (Simões et al. 2015; Inglis et al. 2016; Dominique et al. 2018). Furthermore, making use of QPP statistical studies together with observations of flaring region properties has the advantage of determining scaling laws of QPPs in solar flares (e.g., Pugh et al. 2019), which can help confirm or rule out certain mechanisms. For example, the period of a standing MHD oscillation in a flaring coronal loop should scale with the length of the loop, and hence the period of identified QPPs is expected to be related to flare loop length. Thermal overstability mechanisms similarly generate periods that are determined by the length of the oscillating loop and also plasma temperature (Kumar et al. 2016). In addition to length scales, mechanisms have also been proposed that have a period scaling that depends on the magnetic field strength (e.g., Takasao & Shibata 2016). Other proposed mechanisms require the flare to be accompanied by a coronal mass ejection (CME) and an extended current sheet (e.g., Guidoni et al. 2016; Takahashi et al. 2017); however, to date, the relationship of CME occurrence to the presence of QPPs and their periods has not been established.

In this paper, we present the largest statistical study of QPPs to date, examining all X-, M- and C-class flares observed in the GOES 1–8 Å lightcurves from the last solar cycle (2011–2018). This study builds upon the work of Inglis et al. (2016) to use a Fourier model comparison test to search for evidence of QPPs in flare lightcurves. We use both an active region (AR) and a flare ribbon database (RibbonDB; Kazachenko et al. 2017), and a CME-flare catalog (Akiyama et al. 2019) to compare the periods of QPPs from a subset of the flares analyzed in our survey with both the host flare region properties and the CME association. We also search for differences between QPPs identified during the impulsive and decay phases of the X- and M-class flares.

The paper is structured as follows. In Section 2, the details of the data and the methodology employed for searching for QPPs are described. The results of the large-scale statistical study of QPPs from all flares ≥C1.0 class are presented in Section 3, and the correlations with ribbon properties and CME association are presented in Sections 4 and 5, respectively. Our analysis of the impulsive- and decay-phase QPPs is presented in Section 6. A discussion of the results and a conclusion is presented in Section 7.

2. Data Selection and Methodology

In this study, we searched for the presence of QPPs in the soft X-ray lightcurves from all X-, M-, and C-class solar flares of solar cycle 24 observed by the 1–8 Å channel of the GOES XRS. Compared to other instruments, such as those currently available for hard X-ray and radio observations, which are subject to duty cycles, the GOES XRS provides near continuous measurements of soft X-ray irradiance from the Sun, making it an ideal instrument for statistical surveys of solar flares. Furthermore, with the upgrade to the XRS instrument on board GOES-13, -14, and -15 (which were operational for the past solar cycle), improved soft X-ray measurements became available with a nominal 2 s time resolution, a high signal-to-noise ratio, and a fine digitization, allowing small-amplitude QPPs to be readily detected in both the GOES 1–8 Å and 0.5–4 Å channels (see Dolla et al. 2012; Simões et al. 2015; Hayes et al. 2016, 2019; Dennis et al. 2017; Kolotkov et al. 2018, for recent QPP studies using GOES XRS data). We use GOES-15 XRS data for this study, with supplementary data from GOES-14 for the few events in which GOES-15 data were unavailable.

To compile the flare list for our statistical survey, we queried the Heliophysics Event Knowledgebase to access the GOES flare list produced by NOAA and searched for flares with GOES class ≥C1.0 over the time range of 2011 February 1 to 2018 December 31 (i.e., solar cycle 24) and find a total of 7866 flare events. We then performed a background subtraction for all flares in this list to reclassify the flare intensity. This is required because the background flux levels in the 1–8 Å channel can be at the C1.0 level during days of high activity. To perform the background subtraction, we made use of the TEBBS algorithm (Ryan et al. 2012). After background subtraction, we found that many small C-class flares fall into the B-class category, and we excluded these flares from our analysis.

We used the GOES flare catalog start and end times to determine the time window of the flare to search for signatures of QPPs. The GOES catalog start and end times are defined by NOAA with reference to the measured 1–8 Å channel flux (i.e., not background subtracted). The flare start time is defined as the beginning of the first minute in a sequence of four consecutive minutes of strictly increasing flux in which the last flux value is 1.4 times greater than the first. The end time is defined as the time at which the flux returns to a value that lies halfway between the preflare background level and peak flux values. While these criteria are not always desirable when performing an in-depth analysis of a flaring event, we used them in this study to provide a statistically consistent and reproducible choice of time windows to search for QPPs in the flares. From our background-subtracted flare list, we excluded events that have a flare duration shorter than 400 s, i.e., less than 200 data points, to allow enough Fourier components to be available for our periodogram analysis. After excluding background-subtracted B-class events and the short-duration flares, a total of 5519 flares were left in our compiled database, with the strongest flare being an X9.3.

To detect the presence of QPPs, we used a periodogram-based approach and searched for a significant peak in the Fourier power spectrum of the flare lightcurves. As pointed out in a series of recent studies, the Fourier spectra (i.e., the Fourier power versus frequency) of solar flare lightcurves generally have a power-law shape. This is characteristic of “red noise” as opposed to white noise, which would have a constant power independent of frequency. This must be taken into account when assessing the significance of a peak in a periodogram, as failure to do so may give misleading results or a false detection

5 https://www.lmsal.com/hek/

4 See https://github.com/vasdykov/TEBBS for a Python implementation of this algorithm.
(see Gruber et al. 2011; Inglis et al. 2015; Auchère et al. 2016). For example, when a flaring lightcurve is detrended, which is often performed in the literature to highlight the quasi-periodic variability that lies on a more slowly varying flux, spectral components at longer periods (lower frequency) get suppressed, which can result in the overestimation of the significance of power of the remaining Fourier components. In this work, we utilize the Automated Flare Inference of Oscillations (AFINO) methodology from Inglis et al. (2016) to identify QPPs in the GOES lightcurves (described in detail in Section 2.1). The advantage of this approach is that it can be applied directly to the lightcurves without the need for detrending, thus allowing all Fourier components to be included and the red noise to be fully accounted for. Other techniques, such as that described in Pugh et al. (2017a), also provide a means to detect a periodicity above the red noise in Fourier periodogram analysis. We refer the reader to Broomhall et al. (2019) for a further detailed overview of the different detection techniques for the study of QPPs in solar and stellar flares.

2.1. Automated Flare Inference of Oscillations (AFINO)

The technique of AFINO\(^5\) is described in detail in Inglis et al. (2015, 2016) and is summarized here. The first step is to divide the input time series by the mean and apply a Hanning window function to account for the finite duration of the flaring time series. The Fourier power spectrum of the resulting normalized time series is then computed, different model functions are fit to it, and a model comparison is performed to determine which model best represents the data. In this study, we test the following three functional forms for the power spectra: (1) a power law, (2) a power law with a Gaussian bump added at a particular frequency, and (3) a broken power law. The function with a Gaussian bump is designed to represent a localized enhancement in Fourier power at a particular frequency—i.e., the QPP model. Formally, these functions can be written, respectively, as

\[
M_0(f) = A_0 f^{-\alpha_0} + C_0, \tag{1}
\]

\[
M_1(f) = A_1 f^{-\alpha_1} + B \exp \left( -\frac{(\ln f - \ln f_p)^2}{2\sigma^2} \right) + C_1, \tag{2}
\]

\[
M_2(f) = \begin{cases} A_2 f^{-\alpha_2} + C_2, & \text{if } f < f_{\text{break}}^1 \\ A_2 f^{-\alpha_2-\alpha} f^{-\alpha_3} + C_2, & \text{if } f > f_{\text{break}}^1 \end{cases} \tag{3}
\]

For each model, \(M_i\), \(f\) is frequency, \(\alpha_i\) are the power-law exponents, \(A_i\) are constants, and \(C_i\) are constants for the white noise, which is constant in frequency. The model \(M_1\) is identical to \(M_0\) but with an additional Gaussian bump in log-frequency space at frequency \(f_p\) with a width \(\sigma\) intended to account for enhanced power above the red-noise power-law function. Constraints on these parameters were imposed such that the width of the bump lies within \(0.05 \leq \sigma \leq 0.25\) in log-frequency space, and the peak of the bump, \(f_p\), is restricted to lie within an equivalent period range of \(6 \leq P \leq 300\) s. The time sampling of GOES XRS is 2 s, so 6 s is chosen here as a conservative lower limit, equivalent to 1.5 times the sampling rate, and overlaps with the periods at which QPPs in soft X-ray emission are typically reported (e.g., Simões et al. 2015).

To determine which of these models best fit the Fourier power spectra of the input time series, a model comparison test is performed. First, each model is fit to the data using the functionality within scipy.optimize. Then, the maximum likelihood of this model fit with respect to the data is determined,

\[
L = \prod_{j=1}^{n} \frac{1}{m_j} \exp \left( -\frac{i_j}{m_j} \right). \tag{4}
\]

where \(i = (i_1, \ldots, i_n)\) is the observed Fourier spectrum for a time series of length \(2n\), and \(m_j\) represents the model fit to the data. For each model, this fitting is repeated 20 times with an initial randomized selection of parameters, and the parameters that maximizes the likelihood are kept as the final fit. Once this is determined for each model, the Bayesian Information Criterion (BIC) is used to find which model best represents the data. Mathematically, the BIC is defined such that

\[\text{BIC} = -2 \ln(L) + k \ln(n)\]

where \(L\) is the maximum likelihood of the fit, \(k\) is the number of free parameters of the model, and \(n\) is the number of data points being fit. The BIC criterion is used here to penalize when complexity is added to a model and hence determines if the choice of the QPP model \((M_i)\) with the most parameters is justified. By comparing BIC values of two models, the extent to which a model preferably fits the data can be sought. Because a lower BIC value indicates a preferred model fit, a positive \(\Delta\text{BIC}\) (for \(\Delta\text{BIC} = \text{BIC}_i - \text{BIC}_j, j = 0, 2\)) implies that \(M_i\) fits the data better than model \(M_j\). A value of \(\Delta\text{BIC} \geq 10\) is considered strong evidence in favor of a certain model (Kass & Raftery 1995), and this criterion is used in this work to determine if there is sufficient evidence for the QPP model to be favored.

An additional element of the AFINO methodology is to also calculate a goodness of fit of the models to the data. This is required for cases when no model is appropriate to represent the data and the model comparison has limited value. Following this, a goodness-of-fit statistic (a \(\chi^2\)-like statistic; see Equation (16) of Nita et al. 2014) is calculated for the model fits to the data, and a probability \(p\) that the model fits the data is computed (Equation (18) of Nita et al. 2014). Hence, for a certain flare to be classified as a QPP event, the QPP model had to be strongly favored over the other two model fits (i.e., \(\Delta\text{BIC} \geq 10\)), and the the QPP model has to fit the power spectra with an acceptable probability \(p > 0.01\).

The AFINO technique described here is aimed at searching for a stationary oscillatory signal (i.e., constant period) existing for a large portion of the duration of the flare, or at least with a sufficiently large number of oscillation cycles. This method is hence conservative, but it is a powerful tool to obtain statistically robust, reproducible results and has the ability to correctly identify events consistent with the standard picture of a QPP signature with a very low false-alarm probability (see Broomhall et al. 2019 for a detailed discussion on the performance of AFINO). Hence, the methodology searches for one distinct class of QPPs that are stationary, or weakly nonstationary, that show significantly stable periodic signal throughout the flare. This should be kept in mind when interpreting the results.

\(^5\) https://github.com/aringlis/afino_release_version
3. Statistical Survey Results

The AFINO methodology described above is applied to the 1–8 Å GOES lightcurves of all the flares in our sample. We examine a total of 5519 flares, following the criteria described above, and define flares that have significant evidence of QPPs, i.e., model $M_1$ is preferred and provides an acceptable fit. Examples of the analysis applied to two solar flare events from our sample are shown in Figure 1. The top panel shows an event in which QPPs are detected in the Fourier power spectrum, and the bottom panel shows an event in which no significant enhancement in the power spectrum is identified, and the QPP model is not preferred. In each panel, the input 1–8 Å lightcurve (red) is shown in (a) with the associated time derivative plotted in gray to highlight the variability. The corresponding Fourier power spectra of the red 1–8 Å lightcurves are plotted in black in (b), (c), and (d), and the model fits ($M_0$, $M_1$, $M_2$) are plotted in blue. The dashed gray lines mark the 2.5% and 97.5% quantiles relative to the power-law component of each model to help illustrate enhanced peaks in the spectra. The ΔBIC values are shown in the lower-left corner of (c) for both panels. In the top panel, the QPP model, $M_1$, is found to fit the power spectra best, and the vertical dashed line shows the peak frequency of the enhanced power, in this case 0.034 Hz (i.e., a period of ~29 s).

The detection rate of QPPs as a function of background-subtracted GOES classes is shown in Figure 2. In this plot, the percentage of flares with identified QPPs relative to each flare size bin is shown. The X-class flares are grouped together given the smaller number of events in this class, and similarly, we only break the M classes into two bins, whereas the C-class flares are divided into each subclass. It appears that larger flares have higher occurrence rates of QPPs, with ~46% of X-class flares and ~29% of M-class flares in our sample demonstrating evidence of stationary QPP signatures in their lightcurves. C-class flares, however, have a much lower detection rate at ~7%. Evidently, the larger C-class flares show a higher prevalence rate, and the percentage of detected QPPs reduces for smaller flaring events, with the smallest C1 class events at ~4% (81 flares out of...
2278). The reduced detection rate of QPPs in smaller flares may be due to the fact that smaller flares are indeed less likely to exhibit QPPs. However, these results could also reflect an observational bias, such that the signal in smaller flares is not sufficiently strong to identify the emission variation. In either case, these results show clear evidence that small flares can host QPPs, although it appears to be less common.

The histogram of detected periods of QPPs is presented in Figure 3. The inset plot shows the same data plotted in log space with logarithmically spaced bins. The distribution appears to be log-normal, and there is some apparent skewness associated with the distribution, most probably because of our lower limit cutoff of 6 s. We fit a log-normal distribution (shown by the red dashed curves) to the histogram and find a mean period of 21.6 s. The period of QPPs in soft X-ray emission is within the range of 11.8–39.6 s (one standard deviation of the log-normal fit). This range of periods is consistent with previous smaller-scale statistical studies (e.g., Simões et al. 2015; Inglis et al. 2016), as well as other reports in the literature, even among different spectral bands (e.g., Kupriyanova et al. 2010; Tian et al. 2016; McLaughlin et al. 2018). It is interesting to note that there appears to be a common characteristic timescale among all QPPs, suggestive of a preferred timescale that is probably related to a physical feature prevalent in QPP flares.

We now examine the relationship between the detected QPP periods with both the magnitude of the flare (i.e., GOES class) and the flare duration. This is shown in the form of scatter plots in Figures 4(a) and (b), respectively. There is no correlation found between the GOES class and the QPP period, such that a small C-class flare can host QPPs with the same period as a large X-class flare. This lack of a relationship is similar to other works that have found no (or very weak) correlation between the size of the flare (i.e., GOES class) and QPP period (Inglis et al. 2016; Pugh et al. 2017a; Dominique et al. 2018).

In Figure 4(b), the relationship between QPP period and flare duration is shown. The color of each data point represents the peak flux of each flare, i.e., the GOES class. The flare duration is taken to be the time between the start and end times of the flare defined in the GOES catalog, as described in Section 2, and represents the time interval over which the AFINO analysis was applied. Notably, a positive correlation is identified, and a Spearman rank correlation coefficient of 0.67 is found between the two. This result suggests that longer duration flares host longer period QPPs, and further supports the study of Pugh et al. (2017b, 2019), who found a similar correlation for a smaller sample of flares.

A linear fit (in log space) to the correlation between the flare duration and QPP periods is shown in Figure 4(b). This fit was achieved using a Bayesian linear regression model, using the functionality within pymc3, to estimate the slope and the intercept. The mean values of the fit posteriors are shown in the dashed black line, and the faint gray lines show many samples of the posterior fits. The posterior distributions for the model parameters are normally distributed, and the reported values are the mean of the distribution and the uncertainties are estimated to be the 1σ values. This is given in Equation (B1) with the relationship described as

$$P \propto \tau^{0.67 \pm 0.03},$$

where $P$ is the QPP period and $\tau$ is the duration of the flare. This provides an interesting empirical scaling law of QPPs in soft X-ray flare emission. However, a question arises as to whether this correlation is real or an observational bias such that longer periods cannot be detected in shorter flares. To test this, we follow a similar approach to Pugh et al. (2019) and create a sample of simulated flares with different combinations of flare duration and QPP periods and apply the same AFINO methodology to test for potential biases. The results of our simulated study reveal that the correlation cannot be entirely explained by a bias or selection effect. This study allowed us to identify the region of period and duration combinations where AFINO cannot identify QPPs, which is marked by the gray hatched region in Figure 4(b). It should be noted that the data points that demonstrate the correlation are far from this region. The results of our simulated study also could not explain the absence of short-period QPPs in long-duration flares. Details of this analysis are discussed further in the Appendix A.

4. Relationship with Active Region and Ribbon Properties

We now explore the relationships between the period of the detected QPPs with the properties of the flare AR and ribbons. To achieve this, we combine the results of our statistical survey with the flare ribbon catalog RibbonDB created by Kazachenko et al. (2017). The catalog consists of solar flares greater than C1.0 GOES class that occurred within 45° of the central meridian from 2010 to 2016 April, and hence provides ribbon and AR properties for a subset of the flares analyzed in our statistical survey. The flare ribbon and AR properties provided in this catalog are derived from the 1600 A channel of AIA (Lemen et al. 2012) and HMI magnetogram (Scherrer et al. 2012) observations and include for each flare the location on the visible solar disk, the AR and ribbon areas, the unsigned magnetic flux of both AR and flaring ribbons, and the average magnetic field of both AR and flaring ribbons. A total 2172 events were common between our survey and RibbonDB. Of these, 197 show strong evidence of QPPs.

To determine the relationships between the parameters (listed above) of the flaring ribbon and AR with the period of...
to the bottom right of both scatter plots. This encapsulates information of the breadth of the power enhancement in frequency space of the QPP model, $M_1$. In (a), the period is plotted as a function of peak GOES 1–8 Å X-ray flux. There is no correlation between the two. In (b), we see the relationship between flare duration and period. The color of each data point corresponds to the flare peak flux. The hatched region in the top-left corner shows the region where duration–period combinations cannot be detected. The dashed black line is the linear fit to the data (in log–log space) given by Equation (B1). The Spearman correlation coefficient ($r_s$) and the Pearson correlation coefficient ($r_p$) are labeled in the bottom right of both scatter plots.

Figure 4. Scatter plots of QPP periods with (a) flare size and (b) flare duration. The uncertainties in the periods are based on the width, $\sigma$, of the Gaussian bump, which further explains the correlation between QPP period and these parameters. Overall, when examining all 197 QPP flares, no obvious correlation appears, with corresponding Spearman rank correlation coefficients $r_s \leq 0.16$. If we restrict this analysis to stronger flares with a GOES class greater than M1.0, we begin to identify correlations in the data between the QPP periods and total ribbon area, ribbon unsigned magnetic flux, percentage ratio of ribbon to AR region flux and percentage ratio of ribbon to AR area, all with $r_s \geq 0.44$. The fact that these correlations were only found for larger flares is likely due to the large relative errors in the ribbon measurements for smaller flares in RibbonDB (see Figure 18 of Reep & Knizhnik 2019).

The left- and right-hand panels of Figure 5 show the scatter plots of QPP periods and the ribbon total area, $S_{\text{ribbon}}$, and the ribbon unsigned magnetic flux, $\Phi_{\text{ribbon}}$, respectively. The upper panels show the scatter plot for all flares in the sample, whereas the bottom panels show the scatter plots restricted to X- and M-class flares. The Spearman rank correlation coefficients, $r_s$, and the Pearson correlation coefficients, $r_p$, are indicated in the top left-hand corner of each plot. Fitting the relationships for both $S_{\text{ribbon}}$ and $\Phi_{\text{ribbon}}$ (given by Equations (B2) and (B3)), provides scaling such that

$$P \propto S_{\text{ribbon}}^{0.41 \pm 0.12}$$

and

$$P \propto \Phi_{\text{ribbon}}^{0.40 \pm 0.11}.$$

These positive relationships illustrate that flares with stronger unsigned magnetic flux and larger ribbon areas host longer period QPPs. The remaining scatter plots of the other listed ribbon and AR properties are shown in Appendix C in Figures C1 and C2. We find no correlation between QPP periods and the ribbon and AR average magnetic field, AR area, and AR flux, even when the analysis is restricted to larger flares.

It is particularly desirable to search for correlations between QPP period and the separation of the ribbons, which can be used as an estimate of the flare loop lengths, as scaling relationships between QPP periods and loop length are predicted by some mechanisms, e.g., a standing MHD wave mode. The RibbonDB unfortunately does not include this information; however, another study of Toriumi et al. (2017) has a similar database for flares with a GOES class greater than an M5. From this, we can use the ribbon separation distance and compare with a subset of the flares studied, a total of 21 QPP flares from the sample of 50. We similarly find correlations for ribbon flux and area using this database. But, of particular interest is the relationship between ribbon separation and QPP period, which is shown in Figure 6. This relationship is similarly fit (Equation (B4)), and the scaling for ribbon separation is found to be

$$P \propto d_{\text{ribbon}}^{0.55 \pm 0.15}.$$  

Using the ribbon separation distance as a proxy for loop length, this scaling suggests that longer loop lengths host longer QPP periods, furthering the idea that the QPPs are related to the spatial scale of the hosting flare. This may also explain the relationship between flare duration and QPP periods, such that in longer duration flares continued reconnection occurs at higher and higher altitudes involving longer and longer loops.

These results are consistent with the recent study of Pugh et al. (2019), who found positive correlations between flaring ribbon properties and QPP periods in a study of 22 QPP events from the same AR. It is particularly encouraging that the exponents found here in Equations (6)–(8) are within $2\sigma$ of those found in Pugh et al. (2019). On the other hand, Pugh et al. (2019) also found a strong positive correlation between QPP period and the average ribbon magnetic field, which we do not find here.

5. Relationship to Coronal Mass Ejections

To further understand the flaring conditions necessary to host QPPs, we turn our attention to the relationship between CME association, QPP occurrence rates, and identified periods. To
determine which flares in our sample have an accompanying CME, we make use of the CME-flare list compiled by Akiyama et al. (2019), which includes a list of CMEs associated with solar flares of GOES class greater than M1.0 over the time range of our sample. This CME-flare list is an expanded form of the well-known SOHO/LASCO CME catalog. It consists of a total of 735 flares: 48 X-class and 687 M-class flares. Of these, ~85% of X-class flares and ~45% M-class flares had an associated CME.

To date, it is not yet clear if CMEs play a role in the production of QPPs, and whether an eruption is required for a flare to host QPPs. For example, some proposed mechanisms require a CME in order to generate flare impulsive variability and QPPs (e.g., Takahashi et al. 2017). We begin with testing the occurrence rates of QPPs for both flares that have an associated CME and those that do not. Of the 735 X- and M-class flares, we find that 216 events have QPPs. From the 216 QPP flares, 133 flares (~62%) were associated with a CME, whereas 82 (~38%) flares were not. This illustrates that a CME is not required for a flare to host QPPs, and flares both with and without a CME can have QPP signatures. The higher percentage of CME-related flares is most likely related to the fact that the majority of X-class flares had an associated CME.

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**Figure 5.** Scatter plots of QPP periods with both the ribbon area (left panel) and the ribbon unsigned magnetic flux (right panel) from RibbonDB. For each, the top plot shows the scatter plots for all flares, whereas the bottom plot shows the scatter plots restricted to larger flares (X and M class). The Spearman ($r_s$) and Pearson ($r_p$) correlation coefficients are shown in the top left-hand corner of each plot.

**Figure 6.** Scatter plot of QPP period and ribbon separation with data taken from Toriumi et al. (2017). The Spearman correlation coefficient, $r_s$, is shown in the upper left-hand corner, and a fit to the relations (Equation (8)) is marked by the dashed black line.

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https://cdaw.gsfc.nasa.gov/CME_list/
We now test the detected period distributions for flares with and without a CME. In Figures 7 (a) and (c), we show the distributions of periods for flare events with a CME (red) and flare events with no associated CME (blue), respectively. Interestingly, the two samples have different distributions, but both can be fitted with log-normal Gaussian distributions. Events with CMEs have a spread-out distribution that tends toward longer periods, whereas flares with no CMEs have a more peaked distribution toward shorter periods. Fitting log-normal Gaussian functions to both, we find that CME flares have a mean period of 28.5 s with a range of 11.6–69.7 s within one standard deviation, whereas flares without a CME have a shorter mean period of 17.3 s with a range of 11.9–25.3 s. To further confirm that these distributions are different, we perform a Kolmogorov–Smirnov (K-S) test between the two with a null hypothesis that the two samples are from the same distribution. Performing this yields a K-S statistic of 0.4 and a p-value of $2 \times 10^{-9}$, suggesting that we can reject the null hypothesis and confirm that the two distributions differ.

We now look at the relationship between flare duration and detected QPP periods for both flares with CMEs and those without to test if the duration–period correlation, such as that shown in Figure 4 (b), holds for both cases. For flares with CMEs, we find a strong positive correlation between flare duration and detected period with a Spearman rank correlation coefficient, $r_s$, of 0.80. For flares without CMEs, a weaker positive correlation is still found with a Spearman rank correlation coefficient of 0.41. Fitting a linear model to the correlation, similar to Figure 4 (b), we arrive at the following relationships for both flares with and without a CME, respectively (Equations (B5) and (B6)),

$$P_{\text{cme}} \propto \tau^{0.78 \pm 0.05}$$  \hspace{1cm} (9)

$$P_{\text{nocme}} \propto \tau^{0.35 \pm 0.07}.$$  \hspace{1cm} (10)

These findings suggest different scaling laws for flaring events with and without an associated CME, and perhaps different processes dominate. For events associated with a

Figure 7. Results of QPP flare–CME analysis. (a) and (c) show the histogram of the detected periods for flares with a CME and without a CME, respectively. The dashed curves in each show the log-normal Gaussian fits to the distributions. The QPP period and flare duration relationships for both flares with and without a CME are shown in (b) and (d) respectively.
CME, it is reasonable to assume that reconnection continues at higher altitudes in the trailing current sheet, with longer and longer loop lengths forming as time progresses. This may explain the relationship in Figure 7(b) such that long-duration events evolve to have longer loop length scales and hence longer timescales and QPP periods. For flares without a CME, however, it may be that longer loops do not exist to produce such longer periods, or in fact, a different physical process is dominant for the production of QPPs in these cases.

It is also worth noting that Equation (10) for flares without an associated CME is almost identical to the same-scaling relationship found in Equations (13) and (14) of Pugh et al. (2019). Their study focused on flares from the long-lived AR 12192, which, despite producing a large number of flares, generated relatively few CMEs, with none of the X-class flares having CMEs.

### 6. Impulsive- versus Decay-phase QPPs

In this section, we address the question of whether there is a difference between QPPs detected in different flare phases. It has been demonstrated that QPPs in the decay phase have longer timescales than QPPs in the associated impulsive phase, and there is growing evidence that this is perhaps an inherent feature of flares (Simões et al. 2015; Hayes et al. 2016, 2019; Dennis et al. 2017; Kolotkov et al. 2018). Here we test whether this is true for a large sample of flaring events.

As a step toward a statistical study of this kind, we extend our analysis and methodology to search for differences between the impulsive and decay phases of all the X- and M-class flares in our sample. We achieve this by breaking each flare into two time windows and repeating the AFINO analysis on each section, similar to a windowed Fourier analysis. For the purpose of this study, we defined the impulsive phase as the time between the GOES catalog start time and the time of peak flux in the GOES 1–8 Å channel. For the decay phase, however, we do not use the defined GOES catalog end time as it is known that there is significant observable emission much beyond the GOES-catalog-defined end time. Similarly, we want the time window for the impulsive and decay phases of a flare to be the same so as to avoid introducing any biases. Thus, we defined the end time as the time after the peak flux plus the same interval of time between the start and peak times. This is such that given a start time \( t_s \) and a peak time \( t_p \), the impulsive phase is defined between \( t_s \) and \( t_p \), and the decay phase is defined as the time between \( t_p \) and \( t_p + (t_p - t_s) \). We illustrate this in an example in Figure 8, where both the impulsive and decay phases are highlighted in red and blue, respectively. We exclude events in which the flare impulsive phase (and decay phase) are less than 400 s, leaving a total of 573 flares to be analyzed.

The Fourier power spectrum of both the impulsive and decay phases of each flare in our sample is analyzed by AFINO. We find that 18% of the flares had QPPs in the impulsive phase, 13% had QPPs in the decay phase, and 5% of flares had QPPs identified independently in both. The distribution of detected QPP periods for both the impulsive and decay phases is shown in Figures 9(a) and (b), respectively. These distributions, again log-normal, clearly demonstrate that the decay-phase QPPs have longer periods than do the impulsive-phase QPPs. The mean period, determined from the peak of the Gaussian fit to the distribution, of the impulsive-phase QPPs is 20.7 s with a range of 11.1–38.8 s, whereas the mean period of the decay-phase QPPs is 32.4 with a range of 17.3–60.7 s. It is interesting to note that the impulsive-phase QPP periods overlap with the full statistical study (i.e., Figure 3), and a K-S test suggests that they are from the same distribution (K-S statistic of 0.07 and \( p \)-value of 0.8, meaning we cannot reject the null hypothesis). This is most likely due to the fact that the variability identified in the soft X-ray derivative (or detrended flux) is often observed to have a larger amplitude relative to the overall emission in the impulsive phase compared to the decay phase (e.g., see Hayes et al. 2019). This suggests that AFINO identifies impulsive QPPs in the majority of times when analyzing global flare lightcurves. A K-S test between the impulsive- and decay-phase QPP period distributions suggests that they are from different distributions (K-S statistic of 0.29 and a \( p \)-value of \( 6 \times 10^{-4} \)). Similarly, a K-S test between the...
such that the decay-phase period is longer than the impulsive-phase period. Both phases of the decay-phase QPP distribution and the full flare QPP distribution suggest that they are from two different distributions (a K-S statistic of 0.27 and \(p\)-value of \(6 \times 10^{-4}\)).

We now focus on the events in which QPPs were detected independently in both the impulsive and decay phases. This pertained to 28 events, of which 92% had a longer period in the decay phase than in the impulsive phase. This is illustrated in Figure 10 where the impulsive-phase period, \(P_{\text{impulsive}}\), is plotted against the corresponding decay-phase period, \(P_{\text{decay}}\), for those events where both impulsive- and decay-phase QPPs were identified. As shown, all but two of the points lie above the one-to-one line (black), demonstrating that the decay-phase QPP periods are longer than their associated impulsive-phase periods. Furthermore, for all events in which the decay-phase periods are longer, we fit a linear function (blue dashed line) and find that the \(P_{\text{decay}}\) is typically \(\sim 1.6 P_{\text{impulsive}}\).

These results show that there is a statistical difference between QPPs detected in the different flare phases, implying that this is an inherent feature of flaring QPPs. It should be noted that the number of flares that show QPPs in both phases independently should be considered as a lower limit of evolving QPP signatures. The AFINO methodology is designed to search for global periodic signatures, and hence, if the period is evolving quickly, it will be missed by this technique. The 28 events identified here have very strong stationary features in both phases, which allow them to be detected. The promising results here should now be extended using time-dependent techniques such as wavelet analysis.

7. Discussion and Conclusion

In this paper, we have performed the largest statistical survey of QPPs to date, extending the work of Inglis et al. (2016) to search for the presence of QPPs in the GOES 1–8 A lightcurves of flares from the past solar cycle. We summarize the main findings of our study here:

1. We analyze a total of 5519 flares and find that \(\sim 46\%\) of X-class flares and \(\sim 29\%\) of M-class flares show strong evidence of QPPs. This detection rate is reduced for C-class events where only \(\sim 7\%\) of flares have QPPs.
2. The distribution of QPP periods follows a log-normal distribution centered around 21.6 s, with the majority of events having periods in the range of \(\sim 10–40\) s.
3. No correlation between the flare GOES class and QPP period was found, suggesting that the mechanism that generates QPPs is independent of the flare magnitude and amount of energy released. This result is consistent with stellar flare studies, in which no correlation between QPP period and flare energy was found in a study of Kepler white-light flares that exhibit QPP signatures (Pugh et al. 2016).
4. A positive correlation is found between QPP period and flare duration, such that longer QPP periods are associated with long-duration events. Testing with a set of simulated flares, we conclude that this correlation cannot be fully explained by an observational bias and that the relationship is real.
5. No correlations were found between the global AR properties and QPP periods. This is not surprising and is consistent with Pugh et al. (2017b).
6. For the ribbon properties, correlations were determined for larger flares (X and M classes) between the QPP periods and the ribbon unsigned magnetic flux, total ribbon area, and ribbon separation distance. We determine scaling relationships (Equations (7), (6) and (8)) for these ribbon properties to QPP periods, which agree with the results of Pugh et al. (2019). However, we do not find any correlation between the ribbon average magnetic field and the QPP periods.
7. Flares associated with a CME make up 62% of the detected QPP events for X- and M-class flares, while 38% of the QPP events were from flares without a CME, suggesting that the presence of a CME eruption is not required for the production of QPPs in flaring events.
8. The periods of decay-phase QPPs is statistically longer than the impulsive-phase QPPs. For the majority of events in which QPPs were independently identified in both flare phases, the decay-phase QPP period was 1.6 times the impulsive-phase QPP period.

The results reported in this study represent a conservative estimate of the prevalence of QPPs in solar flares and should be considered a lower limit. The focus of this analysis is to search for significant power in the global Fourier spectra of the flaring lightcurves, and hence an oscillatory signal has to be persistently strong with a stable period throughout the entire event to be detected. Hence, nonstationary QPP events are missed in our study, which again highlights the importance of a classification system for quasi-periodic signatures in solar flares (see Nakariakov et al. 2019).

It is of particular interest that there appears to be a common characteristic timescale universal to flares exhibiting stationary QPPs which may be related to some physical feature of the flaring process. Given that these periods overlap with the expected timescales of MHD wave modes in the solar corona, it is tempting to suggest that the QPPs are related to some resonant MHD wave process occurring in the flaring site. However, much work still needs to be done to explain how various MHD wave modes can produce multiwavelength QPPs, and future forward-modeling efforts are required.

A key finding of this work is the scaling between the flare duration and QPP periods, particularly for the case of flares with associated CMEs. But what could be the cause of such a
relationship? Toriumi et al. (2017) demonstrated that the total duration of a flare is well correlated with the separation of flaring footpoints, or ribbons. These findings are built upon by Reep & Toriumi (2017), where the relationship between duration and ribbon separation is interpreted as being due to the continued reconnection of longer and longer loops that span a flaring arcade. Moreover, the flaring region relationships determined in Section 4 between ribbon properties and QPP periods, particularly the ribbon separation scaling, suggests that ongoing reconnection at increasingly higher altitude producing new, increasingly longer loops could be related to QPPs. In this way, we can interpret the scaling of flare duration and QPP period as a signature of longer loops in later stages of the flare, such that the period evolves to longer timescales when the conditions allow for this to happen, particularly in the case of eruptive flares associated with CMEs. As the reconnection continues, new, longer and longer loops form as the ribbons separate, and hence the timescale of the QPPs increases. This may also help explain the differences between impulsive- and decay-phase QPPs, such that later in the flare, longer periods develop as longer loop lengths exist.

Although this paper does not attempt to distinguish between mechanisms responsible for producing QPPs, the relationships determined here could be utilized by theoretical and modeling efforts to explain the presence of QPPs in solar and stellar flares. For example, the period distribution determined from this large-scale study, as shown in Figure 3, can be used to constrain the timescales of proposed theoretical mechanisms in future parameter studies to ensure that the mechanism can generate the range of observable QPP periods. Moreover, assuming that the QPPs are related to the ongoing process of magnetic reconnection occurring throughout the flare and into the decay phase, the timescales and scaling laws reported in this paper can be used as parameter inputs into global flare models such that each QPP is an energization of a new loop (see Reep et al. 2020 for a detailed use of such approach). From a stellar perspective, on the other hand, the scaling of flare duration and QPP periods determined here (Equation (5)) could be used to compare with the stellar flare observations of QPPs. If a similar scaling did exist in the stellar QPP case, this would further strengthen the argument that stellar QPPs are analogous to solar QPPs, and we can use their observed properties to learn about the local stellar coronal conditions of the flaring AR. With the availability of a large number of stellar flare observations from Kepler, and with the high-cadence observations from TESS coming online soon, systematic searches of these QPP scaling is a particularly interesting avenue of investigation.

L.A.H. is supported by an appointment to the NASA Postdoctoral Program at Goddard Space Flight Center, administered by USRA through a contract with NASA. A.R. I. acknowledges participation in a recent ISSI-Beijing International Team, “Pulsations in solar flares: matching observations and models.” We would like to thank the anonymous reviewer for the positive and encouraging feedback and for the helpful comments which improved this manuscript.

Software: Astropy (Astropy Collaboration et al. 2013), SunPy (SunPy Project et al. 2020), SciPy, Pandas, Matplotlib, NumPy, PyMC3.

Appendix A
Simulated Events Study

To determine the possibility that the strong correlation found between the QPP periods and flare duration in Figure 4 is influenced by an observational bias and/or a result of limitations of the AFINO detection method, we perform a simulated study to generate a large sample of flares with varying flare durations and QPP periods, and use the same methodology to detected the simulated QPPs. To achieve this, we follow the work of Pugh et al. (2019) and generate 4096 flares with 16 different flare durations, QPP periods, and durations of flares in which the QPP was present. The flare durations were in the range of 400–26,000 s, the QPP periods in the range 6–300 s, and QPP durations in the range 200–2600 s. Their values were then selected from these values uniformly distributed in log space.

The flare background was built using the elementary flare model from Gryciuk et al. (2017), such that the soft X-ray flux lightcurve can be described as

\[
 f_{\text{sxr}}(t) = \frac{1}{2} \pi A C D \exp \left[ -\left( B - t \right) + \frac{C^2 D^2}{4} \right] \times \left[ \text{erf}(Z) - \text{erf} \left( Z - \frac{t}{C} \right) \right]. \tag{A1} 
\]

where \( A, B, C, \) and \( D \) are constants that determine the shape and

\[
 Z = \frac{2B + C^2D}{2C} \tag{A2} 
\]

Following Pugh et al. (2019), these arbitrary parameters were set to \( A = 1, B = \tau_{\text{flare}}/15, C = \tau_{\text{flare}}/10, \) and \( D = 3/\tau_{\text{flare}}. \) We model the QPP signal as a sinusoid modulated by a Gaussian described as

\[
 f_{\text{qpp}}(t) = A_{\text{qpp}} \cos \left( \frac{2\pi t}{P} \right) \exp \left( -\frac{(t - t_0)^2}{\tau^2/2} \right). \tag{A3} \]

For our simulated flare examples, we normalize the flare signal, \( f_{\text{sxr}} \), and add the QPP signal, \( f_{\text{qpp}}, \) which is taken to be 1% of the total flare. We also add white noise on the order of 0.01%, which is typical for GOES XRS observations (e.g., Simões et al. 2015). We then analyze this set of simulated flares with AFINO and attempt to detect the presence of the simulated QPP and search for the same relationship between QPP period and flare duration. The results of this are shown in Figure A1.

**Figure A1.** Results of the simulated flare study. Here, the detected QPPs in the simulated flare sample are shown as a scatter plot of flare duration and QPP period.
From this, we can clearly identify a region of long-period, short-duration flares that are not detected to have QPPs even though QPPs exist in this sample (i.e., the top left-hand corner). This region is shown in the top-left corner of plots of QPP period and flare duration in Figures 4 and 7. Furthermore, there is no absence of detection in the short-period, long-duration simulated flares unlike the observed case, strengthening the possibility that the observed correlation is not a result of observational bias. Hence, the results of the simulated events study demonstrate that the measured correlation is a true relationship and not an artifact of the detection method or of observational bias.

**Appendix B**

**Scaling Equations**

Here we list the fits of the relationships of the QPP periods and different flaring parameters. The scaling equations below, Equations (B1), (B2), (B3), (B4), (B5), and (B6), correspond to the fits shown in Figures 4(b), 5(a), 5(b), 6, 7(b), and 7(d), respectively.

\[
\log P = (0.67 \pm 0.03) \log \tau_{\text{flare}} - (0.68 \pm 0.09), \quad (B1)
\]

\[
\log P = (0.41 \pm 0.12) \log S_{\text{ribbon}} - (6.40 \pm 2.32) \quad (B2)
\]

\[
\log P = (0.40 \pm 0.11) \log \Phi_{\text{ribbon}} - (7.30 \pm 2.44) \quad (B3)
\]

\[
\log P = (0.55 \pm 0.15) \log d_{\text{ribbon}} + (0.7 \pm 0.27) \quad (B4)
\]

\[
\log P_{\text{cme}} = (0.78 \pm 0.05) \log \tau_{\text{flare}} - (1.02 \pm 0.17) \quad (B5)
\]

\[
\log P_{\text{nocme}} = (0.35 \pm 0.07) \log \tau_{\text{flare}} - (0.22 \pm 0.21). \quad (B6)
\]

**Appendix C**

**Additional Figures**

Here we show the remainder of the correlation scatter plots from Section 4. Figure C1 shows the other scatter plots of the ribbon properties and QPP periods. Figure C2 shows the scatter plots of the AR properties and the QPP periods.

![Figure C1](image1.png)

**Figure C1.** Scatter plots of other flaring parameters from RibbonDB (Kazachenko et al. 2017). The top panels show all the flares with detected QPP that overlap with the RibbonDB, and the bottom panels show only the X- and M-class flares, similar to Figure 5. The left-hand panel shows the correlation of QPP period to the percentage of ribbon area to AR area, and the middle panel shows the correlation of QPP period to the percentage of reconnecting flux to AR flux. For the X- and M-class flares, it is clear that there is a positive correlation for both of these. The right-hand panel, however, shows the relationship between QPP period and average ribbon magnetic field, in which no correlation is apparent.
Figure C2. Scatter plots of other AR parameters from RibbonDB (Kazachenko et al. 2017) that show no significant correlations with QPP periods. The top panels show all the flares with detected QPP that overlap with the RibbonDB, and the bottom panels show only the X- and M-class flares, similar to Figure 5. The AR total area, AR total magnetic flux, and AR average magnetic field scatter plots with QPP period are shown in the left-hand, middle, and right-hand plots, respectively.

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