When NAS Meets Trees:
An Efficient Algorithm for Neural Architecture Search

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Abstract

The key challenge in neural architecture search (NAS) is designing how to explore wisely in the huge search space. We propose a new NAS method called TNAS (NAS with trees), which improves search efficiency by exploring only a small number of architectures while also achieving a higher search accuracy. TNAS introduces an architecture tree and a binary operation tree, to factorize the search space and substantially reduce the exploration size. TNAS performs a modified bi-level Breadth-First Search in the proposed trees to discover a high-performance architecture. Impressively, TNAS finds the global optimal architecture on CIFAR-10 with test accuracy of 94.37% in four GPU hours in NAS-Bench-201. The average test accuracy is 94.35%, which outperforms the state-of-the-art. Code is available at: https://github.com/guochengqian/TNAS.

1. Introduction

Neural architecture search has spurred increasing interest in both academia and industry for its ability in finding high-performance neural network architectures with minimal human intervention. To achieve the most accurate NAS algorithm, one can explore all candidate architectures, training each one to convergence, and picking the best-performing architecture. However, this brute-force NAS is infeasible due to the enormous search space. Therefore, one of the key questions towards a successful NAS algorithm is: how to efficiently explore the search space?

One-shot NAS [6, 27, 3, 24] impressively improved the efficiency of NAS. One-shot NAS leverages a weight-sharing strategy and approximately trains only one network, called the supernet, which subsumes all candidate architectures. Each candidate architecture directly inherits weights from the supernet without training. Despite the efficiency of one-shot NAS algorithms, they incur architecture evaluation degradation, i.e. the architecture performance evaluated using the weight-sharing is not correct, which leads to a degraded search accuracy [38, 21].

In this work, we diverge from the paradigms set by early NAS, and instead design a new algorithm to explore the search space in a wiser manner. Consider a search space $A$ where the number of candidate operations is $M$ and the number of architecture layers to search is $L$. The size of the entire search space $|A|$ equals to $M^L$. If $M = 2$ or $L = 1$, $|A|$ can be drastically reduced to $2^L$ or $M$. The intuition
behind our work is to develop a method that factorizes the operation space (size $M$) and the architecture layers (size $L$), and thus reduces the exploration size exponentially.

**Contributions.** (1) We introduce an architecture tree and a binary operation tree to factorize the search space $L$ and $M$, respectively. By combining the two trees, we iteratively branch a search space into two exclusive subspaces. (2) We propose a novel, flexible, accurate, and efficient NAS algorithm, called **TNAS**: NAS with trees. TNAS performs a modified bi-level Breadth-First Search (BFS) in the two proposed trees. By adjusting the expansion depths of the BFS, TNAS explicitly controls the exploration size $N$ and is able to exponentially reduce $N$ from $M^L$ to $O(L \log_2 M)$. The essence of TNAS is illustrated in Figure 1. (3) TNAS is is able to find the global optimal architecture on CIFAR-10 [18] (94.37% test acc.) in NAS-Bench-201 [13] within 4 GPU hours on one GTX2080Ti GPU. TNAS outperforms the RL and EA based NAS [45, 28] as well as one-shot NAS [27, 9], with a similar search cost.

2. Related Work

The computational bottleneck of NAS is exploring candidate architectures in this huge search space and exploiting each one (i.e. score the architecture by training to convergence). Through the work, we name the number of architectures to score as the exploration size, denoted as $N$. To alleviate the computational bottleneck, NAS algorithms should consider: (i) how to explore wisely, where time can be saved if the algorithm explores more among the “good” architectures and less on the “bad” ones, and (ii) how to exploit wisely, where training each network to convergence just to know the architecture’s performance then throwing weights away is inefficient.

**Explore wisely.** Early methods adopt Reinforcement Learning [44, 2, 45] or Evolutionary Algorithms [30, 29, 28] to auto-explore the huge search space. Although early NAS methods have been able to discover architectures that outperform manually designed networks, they consume significant computational resources. This is primarily because these algorithms require a large exploration size to achieve a decent search accuracy. Progressive NAS is a method that factorizes the search space into a product of smaller search spaces and can greatly reduce the exploration size. PNAS [23] and P-DARTS [9] start searching with shallow models and gradually progress to deeper ones. Li et al. propose block-wise progressive NAS [19, 20] that consider the architectures is built by sequential blocks and search the architecture block by block. SGAS [21], GreedyNAS [36], and [17, 41, 34] progressively shrink the search space by dropping unpromising candidates. These progressive NAS methods require a much smaller exploration size, but their greedy nature hampers their search accuracy. Our TNAS designs a new paradigm for exploring wisely by introducing two trees to factorize the search space.

**Exploit wisely.** A straightforward idea of reducing exploitation is to train fewer epochs as done in Block-QNN [42]. A more advanced solution is to share weights among child networks, apart from training them from scratch. This weight-sharing strategy was first proposed by ENAS [6, 27] and has inspired many following works, including one-shot NAS [3, 24, 15, 32, 26, 37, 10, 14]. To alleviate the evaluation degradation [38, 4, 21] issues of one-shot NAS caused by weight-sharing, few-shot NAS [40, 31] were proposed by training $k$ supernets instead of training only one. Another line of work to exploit wisely is accuracy prediction [23, 11, 43], where an accuracy predictor is learned to directly estimate an architecture’s accuracy without training it completely. Recently, metric-based NAS methods [25, 8, 1, 39, 17, 7] have emerged, using well-designed metrics to score the sampled architectures quickly with significantly less training or even no training. Since our paper focuses on how to wisely explore the NAS search space, wise exploitation is an orthogonal direction. In fact, we highlight here that our TNAS can be applied with nearly all the aforementioned exploit-wise NAS methods.

3. Methodology

We present TNAS (NAS with trees) to efficiently find a high-performance architecture by performing a modified bi-level Breadth-First Search in the proposed architecture tree $T_A$ and binary operation tree $T_O$.

3.1. Architecture Tree $T_A$

Given a search space with $L$ layers and $M$ operations per layer, we propose an architecture tree $T_A$ to factorize the one-shot architecture and to exponentially reduce the exploration size. The architecture tree $T_A$ is illustrated in Figure 2(a). Each node in the tree represents an architecture. The root node is the $M$-path $L$-layer one-shot architecture. Each path in a layer denotes a distinct operation from $M$ candidate operations. $T_A$ has a maximum depth level equal to $L$. For each node (architecture) at depth $i$ ($i \in [0, 1, \ldots, L-1$), the tree separates the $M$ operations in layer $i$ into $M$ branches each with a single operation. Such branching is repeated for each node, until the leaf nodes are reached. Each leaf node represents a distinct single-path architecture. The union of the leaf nodes is the set of all candidate architectures. Note that if layer $i$ contains multiple operations, the output of this layer will be the summation of the outputs of all operations at this layer, as inspired by the one-shot NAS [3] and is formulated as:

$$\bar{o}^i(x) = \sum_{o_j \in \mathcal{O}} o_j^i(x),$$  \hspace{1cm} (1)
The binary operation tree \( \mathcal{T}_O \) and the proposed Breadth-First Search (BFS).

where \( \mathcal{O} = \{ o_j \mid j = 1, 2, \ldots, M \} \) denotes \( M \) different operations and \( x \) denotes the input feature map.

Breadth-First Search (BFS) in \( \mathcal{T}_A \). Here, we show that the architecture search can be done by performing our modified BFS in the architecture tree \( \mathcal{T}_A \). Our BFS requires a hyperparameter, the expansion depth denoted as \( d_a \), where the subscript \( a \) denotes “architecture”. BFS starts at the root node (the one-shot model) at depth 0, expands all its successors until depth \( d_a \), and obtains up to \( M^{d_a} \) leaf nodes after expansion. BFS scores the leaf nodes by these leaf nodes, and picks the node with the highest score as the root node for the next step. The above procedure is defined as a decision step, and is repeated until a single-path architecture is determined. The score function can be chosen to be the validation performance after training, or a metric function proposed by any metric-based NAS method such as the number of linear regions [25]. For simplicity, we choose the scoring function to be validation performance in our experiments. The expansion depth \( d_a \) of the BFS denotes how many layers to branch at each decision step. As illustrated in Figure 2(b), the BFS with \( d_a = 1 \) is a sequential, greedy NAS algorithm that decides the operation for the architecture layer by layer, similar to the progressive NAS method SGAS [21]. The BFS with \( d_a = L \) as shown in Figure 2(c) works as the brute-force NAS, where only 1 decision step is required. The BFS explores all \( M^L \) subnets and decides the operation for all of the layers at the same decision step. When \( d_a = k \in \{ 2, \ldots, L - 1 \} \), \( k \) layers are branched in each decision step, \( M^k \) subnets need to be scored, and \( \left\lceil \frac{L}{k} \right\rceil \) decision steps are required. This case works similar to the block-wise NAS [19], while our BFS does not require any block-level supervision.

3.2. Binary Operation Tree \( \mathcal{T}_O \)

We propose a binary operation tree \( \mathcal{T}_O \) that hierarchically factorizes the operation space to further reduce the exploration size. Each node in \( \mathcal{T}_O \) is an operation group consisting of one or more distinct operations. The root node represents \( \mathcal{O} \), the entire operation space containing all \( M \) operations. \( \mathcal{T}_O \) starts from the root node and branches it into two child nodes that represent two exclusive operation groups. Such branching is repeated for each node until a leaf node that represents a single operation is reached. \( \mathcal{T}_O \) has \( M \) leaf nodes. The union of leaf nodes is \( \mathcal{O} \). Taking NAS-Bench-201 [13] operation space as an example, we illustrate the \( \mathcal{T}_O \) in Figure 3.

Breadth-First Search (BFS) in \( \mathcal{T}_O \). The expansion depth of our modified BFS in \( \mathcal{T}_O \) is denoted as \( d_o \). BFS starts at the root node (the entire operation space) at depth 0, expands all its successors until depth \( d_o \), and obtains up to \( 2^{d_o} \) leaf nodes after expansion. These leaf nodes represent the current candidate operation groups. BFS scores the architectures equipped with these different operation groups, and picks the node defined by the operation group with the highest score as the root node for the next stage. The above procedure is defined as a decision stage, and is repeated until a single operation is picked. Note that each architecture layer can choose different operation groups at each decision stage. If \( d_o = 1 \), the BFS decides the operation groups per depth following \( \mathcal{T}_O \). In this case, BFS consists of \( \left\lceil \frac{\log_2 (M-1)+1}{d_o} \right\rceil = 3 \) decision stages. At the 1st stage, BFS decides among None or Not None for each architecture layer. At the 2nd stage, for those layers that chose Not None, the algorithm decides among the Convolution group.
or Topology group. At the final stage, the algorithm will pick a single operation for each layer. If $d_o = 3$, BFS only needs one decision stage to decide which single operation to choose for each layer.

### 3.3. TNAS

We present a new NAS algorithm: Neural Architecture Search with Trees (TNAS). Given a search space with $M$ candidate operations and $L$ layers, TNAS constructs a binary operation tree $T_O$ and an architecture tree $T_A$. TNAS starts from the $M$-path $L$-layer one-shot model, and performs bi-level Breadth-First Search on $T_O$ and $T_A$. At the outer loop, TNAS performs BFS with the expansion depth $d_o = 1$ on $T_O$ by default, to make a large $d_o$ feasible. The outer loop requires $\log_2 (M - 1) + 1$ decision stages. Each stage branches each operation group of the chosen layers into two child operation groups, which define the operation search space for the inner loop. The outer loop repeats the decision stage until every architecture layer reaches a leaf node of $T_O$, i.e. all the layers pick a single operation. In the inner loop, TNAS performs BFS with an expansion depth $d_a$ on $T_A$. The inner loop takes $\left\lceil \frac{L}{d_a} \right\rceil$ decision steps. Each step chooses $d_a$ undecided layers to branch, obtains $2^{d_a}$ subnets, scores each subnet, and then chooses the highest scoring one. The chosen subnet will be used to replace the one-shot model and become the starting point for the next step. The inner loop repeats the above decision step until it chooses a leaf node of $T_A$, i.e. all layers of the architecture have decided their operation group at the current decision stage. We illustrate the TNAS algorithm ($d_o = 1, d_a = 2$) in Figure 4. The NAS-Bench-201 [13] search space (i.e. $M = 5$ and $L = 6$) is used as an example.

#### Exploration size analysis.

Given a search space with $M$ operations and $L$ layers, TNAS reduces the exploration size exponentially from $M^L$ to:

$$N = O \left( 2^{d_o} \times \left\lceil \frac{L}{d_a} \right\rceil \times \frac{\log_2 (M - 1) + 1}{d_o} \right)$$

### 4. Experiments

**Setup.** We evaluate TNAS on NAS-Bench-201 [13] with $(d_o = 1, d_a = 6)$. We train each architecture over 2 epochs and use the top-1 accuracy on validation set as the score for the architecture. If the architecture consists of a layer with multiple operations, the output of this layer is the sum of all outputs as Equation 1. Note that other scoring methods aforementioned in Section 2 can also be applied.

**Results.** Table 1 compares TNAS with SOTA. TNAS finds the global optimal architecture in CIFAR-10 [18] within 4 GPU hours. TNAS achieves 94.35% average test accuracy, outperforming all other NAS methods. We highlight that TNAS outperforms the REA [28], REINFORCE [35] and random search (RS [5]) with a similar search cost, which clearly demonstrates the benefit of our NAS paradigm. TNAS also performs significantly better than the one-shot based methods, such as ENAS [27], GDAS [12] and DARTS [10], while being more efficient.

### 5. Conclusion

We present a novel NAS algorithm, TNAS, that performs bi-level BFS on the proposed binary operation tree and the architecture tree. By adjusting the search depths on the trees, TNAS can explicitly control the exploration size. TNAS finds the global optimal architecture in NAS-Bench-201 [13] with a search cost of less than 4 GPU hours.

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