A central unresolved issue of high temperature superconductivity is the connection of normal state correlations, referred to as the pseudogap [1], to the origins of high-\(T_c\). At the heart of the debate [2] is whether the pseudogap, which manifests itself as a depletion of the quasiparticle density of states (DOS) below a characteristic temperature \(T^*\), originates from spin or charge degrees of freedom and, in particular, whether it derives from some precursor of Cooper pairing [12] that acquires the superconducting coherence at \(T_c\). Energies of the order of the pseudogap have been accessed with elevated temperatures, with applied voltage in tunneling measurements, and with infrared frequencies in optical spectra [1]. But little is known about the effect of magnetic field. The magnetic field response may be unique: e.g., in the case of the superconducting state the upper critical field \(H_{c2}\) is determined by the superconducting coherence length, and not directly by the superconducting gap, since magnetic field strongly couples to the orbital motion of Cooper pairs.

Current knowledge about the field dependence of the pseudogap derived from spectroscopic measurements is partly limited by the available dc field range [2]. More importantly, there is no systematic doping dependence in a single family of cuprates. Even in optimally doped \(\text{YBa}_2\text{Cu}_3\text{O}_{7-\delta}\) alone, based on NMR relaxation rate measurements below 27.3 T, the pseudogap was claimed to decrease [2] or be independent of magnetic field [3]. In the underdoped \(\text{YBa}_2\text{Cu}_3\text{O}_8\) no field effect on \(T^*\) was reported up to 23.2 T [3], while a recent NMR study indicated a measurable field dependence in slightly overdoped Ti\(\text{Sr}_2\text{CaCu}_2\text{O}_{6.8}\) [10]. In this paper, we report the interlayer (\(c\)-axis) resistivity \(\rho_c\) measurements in fields up to 60 T in \(\text{Bi}_2\text{Sr}_2\text{CaCu}_2\text{O}_{8+y}\) (BSCCO) crystals in a wide range of doping, from which we make a first systematic evaluation of the pseudogap closing field \(H_{pg}\) that restores DOS to its ungapped state. Our results indicate a pronounced difference between field-temperature (\(H-T\)) diagrams of the pseudogap and the superconducting states and a simple Zeeman scaling between \(H_{pg}(0)\) and \(T^*\).

Among various techniques that quantify DOS, the \(\rho_c\) measurements are uniquely suited for exploring the highest magnetic field range available only in a pulsed mode. In highly anisotropic materials such as BSCCO where interlayer coupling between \(\text{CuO}_2\) layers is sufficiently weak, the \(c\)-axis transport directly measures Cooper pair or quasiparticle tunneling in both normal and superconducting states [4], providing bulk information about the quasiparticle DOS at the Fermi energy. Thus, \(\rho_c\) should be particularly sensitive to the onset of the pseudogap formation, since the DOS depletion is largest at the Fermi energy. Moreover, \(\rho_c\) is controlled by the (\(\pi, 0\)) points (‘hot spots’) on the anisotropic Fermi surface [14,15], where the pseudogap first opens up [1]. (This is in contrast to the in-plane resistivity \(\rho_{ab}\) mainly determined by carriers with momenta along the (\(\pi, 0\)) directions [4].)

Our task here is to map \(H-T\) diagram of the pseudogap state. To elucidate the field dependence of the pseudogap over a wide doping range, we carefully adjusted hole concentration \(p\) spanning both underdoped and overdoped regimes in BSCCO crystals grown by the floating-zone method [16]. The doping level was controlled by annealing in \(\text{O}_2\) or \(\text{N}_2\) at the appropriate pressures [2]. \(\rho_c(H)\) was measured using a 33 T dc magnet [17] and a 60 T long pulse (LP) system at the National High Magnetic Field Laboratory (NHMFL) [18].

In slightly underdoped BSCCO at temperatures below \(T_c\), the field dependence of \(\rho_c\) exhibits a peak that we have previously demonstrated to arise from a competition between two tunneling conduction channels: of Cooper pairs (at low fields) and quasiparticles (mainly at
The peak position marks the field (in the superconducting state) where the quasiparticle contribution overtakes the Cooper pair tunneling current. The doping dependence of $\rho_c(H)$ in Fig. 1 clearly shows that the peak field $H_{sc}$ in the highly underdoped crystal, where interlayer (Josephson) coupling is the weakest, is most easily suppressed. Magnetoresistance (MR) above $H_{sc}$ is negative and remains so above $T_c$, as has been seen at lower fields [13]. An important difference between the underdoped and overdoped regimes is in the slope of the negative MR. A gentle slope in the underdoped regime turns steeper in the overdoped regime and, as shown in Fig. 1(c), at the highest fields the low-temperature $\rho_c(H)$ rapidly approaches the normal-state value.

In the overdoped samples, negative MR eventually disappears. This occurs at the same temperature at which the zero-field $\rho_c(T)$ develops a characteristic upturn from the $T$-linear dependence of the metallic state [Fig. 2(a)]. This temperature – at which a gap-like feature also appears in the static susceptibility [3] and in the tunneling spectra [4] of BSCCO – is identified as the pseudogap temperature $T^*$. In the pseudogap state below $T^*$, the negative MR is naturally understood by the suppression of the pseudogap by magnetic field [21]. In our most overdoped crystal with $T_c = 67$ K, a magnetic field of $\sim 60$ T downshifts the $\rho_c(T)$ upturn and the associated $T^*$ by about 20 K [Fig. 2(b)]. In other words, at this doping level, the 60 T field at $\sim 100$ K closes the pseudogap.

To track the pseudogap closing field at lower temperatures, we consider the excess resistivity $\Delta \rho_c$ due to the DOS depletion. It is known from the intrinsic tunneling spectroscopy measurements [3] that the $T$-linear dependence of the metallic state persists below $T^*$ for bias voltages sufficiently above the pseudogap voltage. Subtracting this metallic contribution gives $\Delta \rho_c$. $\Delta \rho_c$ at which $\Delta \rho_c$ vanishes is the pseudogap closing field $H_{pg}(T)$. To obtain $H_{pg}(T)$, we first note that the $c$-axis MR in the pseudogap state was recently shown to follow a power-law field dependence up to 60 T [14]. A fit to the power-law field dependence of $\Delta \rho_c(H)$ at different temperatures [inset in Fig. 2(b)] allows us to evaluate $H_{pg}(T)$ beyond 60 T. This evaluation is insensitive to the detailed functional form of the fit, as can be inferred from Fig. 1(c). We tried other extrapolation fits (e.g. polynomial) and they gave the same values of $H_{pg}(T)$ within the error bars in Fig. 3(a).

The entire $H$-$T$ diagram of the pseudogap in the overdoped crystal is shown in Fig. 3. At low temperatures $H_{pg}$ is essentially flat with the limiting value of $\sim 90$ T. This is in marked contrast with the characteristic fields of the superconducting state: the peak field $H_{sc}(T)$ and the irreversibility field $H_{irr}(T)$. At low temperatures $H_{sc}(T)$ grows exponentially and points to the zero-temperature value of $\sim 100$ T, nearly independent of doping [Fig. 3(b)]. This difference, consistent with recent NMR [8] and intrinsic tunneling measurements [11], may indicate different origins of the pseudo- and superconducting gaps.

In the overdoped crystals the low-temperature $H_{pg}$ and the zero-field $T^*$ can be obtained independently and the comparison between the two (Fig. 4) leads to a strikingly simple conclusion. The pseudogap closing field scales with $T^*$ as $g\mu_B H_{pg} \approx k_B T^*$. Here $g$-factor $g = 2.0$, $\mu_B$ is the Bohr magneton, and $k_B$ is the Boltzmann constant. This immediately suggests that magnetic field couples to the pseudogap by the Zeeman energy of the spin degrees of freedom. In the overdoped regime, the appreciable error bars in $H_{pg}$ reflect the fact that the extrapolation extends considerably beyond the maximum laboratory field range of 60 T [inset of Fig. 1(c)]. However, the estimate gives a consistent and physically sensible picture, since in the overdoped regime we find that below 150 K $H_{pg}(T)$ is also flat and $H_{pg}(p)$ is a smooth continuation from the overdoped side. The observed general trend of the high-field slope of $\rho_c(H)$ as a function of doping is unmistakable, and the Zeeman energy scale of $H_{pg}$ is in good agreement with the reported energy scale of the pseudogap and $T^*$ [22] (see the shaded band in Fig. 4). Thus, we surmise that the Zeeman scaling found in the overdoped samples holds in the entire doping range.

In contrast to $H_{pg}(p)$, the doping dependence of the peak field $H_{sc}$ is weak and roughly follows a parabolic dependence similar to $T_c(p)$. Note that $H_{sc}$ does not represent an upper critical field $H_{c2}$. The boundary at $H_{c2}$ in high-$T_c$ superconductors is a fuzzy crossover difficult to estimate [23], but should be higher than $H_{sc}$ [3]. If strong phase fluctuations associated with the precursor superconductivity are responsible for the pseudogap state [2], one would expect $H_{pg} \gg H_{c2} \gtrsim H_{sc}$ in the zero-temperature limit since quantum phase fluctuations should also be significant. In the overdoped regime, the difference between $H_{pg}$ and $H_{sc}$ in the low temperature limit is huge, which in this scenario can be attributed to quantum fluctuations. Surprisingly, in the overdoped regime, while the pseudogap region in the $H$-$T$ diagram is still nontrivially large, the low temperature values of $H_{pg}$ and $H_{sc}$ are nearly the same, which may raise questions about large quantum fluctuations.

Our finding that Zeeman splitting closes the pseudogap implies that the triplet spin excitation at high fields overcomes the singlet pair correlations responsible for the gap in the spin spectrum, and that the orbital contribution is very small. In preformed pair scenarios, our results would require pairing correlations on relatively short length scales with negligible orbital motion of pairs. This may be satisfied in a class of models, where charges (holes) self-organize into micro-stripes below $T^*$ [24,25]. The mechanism of pairing is the generation of the ‘spin-gap’ in spatially confined Mott-insulating regions with local antiferromagnetic correlations in the proximity of the metallic stripes [4]. However, any future theoretical input must reconcile such pairing with a lack of signifi-
quant quantum fluctuations in the overdoped regime.

A spin-gap in a doped Mott insulator also appears in resonating-valence-bond theory, where the spin and charge degrees in the CuO$_2$ plane are separated into ‘spinons’ and ‘holons’ [28]. Studies based on this idea [24–27] derive a doping-dependent spin-gap temperature evolving from zero on the overdoped side to a finite value prescribed by the antiferromagnetic exchange $J$ ($\sim 1000$ K) as $p \to 0$. This spin-gap temperature corresponds to the formation of spinon singlet pairs. A gap in the spin excitation spectrum can be seen in the c-axis tunneling spectra, since during the interplane tunneling process spinons and holons recombine into conventional carriers with charge and spin. Our empirical linear scaling of $H_{py}(p)$ and $T^*(p)$ gives an energy scale $\sim 930$ K in the $p \to 0$ limit, of the order of $J$.

Our results up to 60 T point to a predominant role of spins in the formation of the pseudogap consistent with models based on a doped Mott insulator [24–27]. An interesting issue concerns the existence of a quantum critical point at which the pseudogap temperature goes to zero [25]. This has been argued to occur at a critical doping $p \approx 0.19$. However, our most overdoped crystal with $p \approx 0.22$ has the pseudogap still unmistakably prominent [28], likely reflecting higher sensitivity of the interlayer tunneling at $(\pi, 0)$ points on the Fermi surface [14–15], where a spectral weight depletion onsets at a higher temperature [16].

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FIG. 1. c-axis resistivity $\rho_c$ (labeled by temperatures) vs magnetic field $H(\parallel c)$ in an underdoped (UD) BSCCO crystal (a) and two overdoped (OD) crystals (b), (c). In the superconducting state, $\rho_c(H)$ becomes finite above the irreversibility field $H_{irr}$ and exhibits a peak at $H_{sc}$. The core feature in $\rho_c(H)$ that changes with doping is the slope of the high-field negative MR. Dotted lines in (c) are guide to the eye pointing to the limiting value ($< 100$ T) of $H_{pg}(T)$. Inset: Excess resistivity due to the pseudogap $\Delta \rho_c$ (see Fig. 2) as a function of field for two samples at $T \sim 0.2T^*$. Thin lines are power-law fits and the shades indicate the uncertainties estimated from the leeway in the fitting parameters.

FIG. 2. Determination of the pseudogap temperature $T^*$ and the pseudogap closing field $H_{pg}$ from $\rho_c(T, H)$ in overdoped BSCCO. (a) $\rho_c(T)$ deviates from metallic $T$-linear dependence at the same temperature where negative MR disappears, identified as pseudogap temperature $T^*$. (b) In our most overdoped BSCCO with $T_c = 67$ K, $T^*$ is shifted by $\sim 20$ K by a 58.5 T field. Inset: The excess quasiparticle resistivity $\Delta \rho_c(H)$ (above $H_{sc}$) is fitted to a power-law field dependence $[\Delta \rho_c(H) - \Delta \rho_c(0)] \propto H^\alpha$. 
FIG. 3. \(H-T\) diagram showing the pseudogap closing field \(H_{pg}(T)\), the peak field \(H_{sc}(T)\), and the irreversibility field \(H_{irr}(T)\) in the overdoped BSCCO. (a) Up to 60 T, \(H_{pg}(T)\) is directly determined from the down-shifting upturn of \(\rho_c(T)\) (red squares). At lower temperatures, \(H_{pg}(T)\) is obtained by extrapolating \(\Delta\rho_c(H)\) to zero [inset in Fig. 2(b)]. The two procedures consistently produce a seamless \(H_{pg}(T)\) within the error bars. The starkly different temperature dependencies of \(H_{pg}(T)\) and \(H_{sc}(T)\) \(\leq H_{c2}\) here extrapolate to roughly the same zero-temperature value. The usual estimate \(H_{c2}(0) = 0.7(\partial H_{c2}/\partial T)|_{Tc}\) with an initial slope of \(\sim 2\) T/K [13] gives \(H_{c2}(0) \approx 94\) T, very close to the value of \(H_{sc}(0)\). (b) At low temperatures, \(H_{sc}(T)\) grows nearly exponentially and, in the \(T \to 0\) limit, is only weakly dependent on doping.

FIG. 4. Doping dependencies of low-temperature \(H_{pg}\), \(H_{sc}(T \to 0)\), \(T^*\), and \(T_c\). The hole concentration \(p\) was obtained from the empirical formula \(T_c/T_{c,max} = 1 - 82.6(p - 0.16)^2\) [29] with \(T_{c,max} = 92\) K. The right-hand-side field scale directly translates onto the Zeeman energy scale on the left-hand-side as \((g\mu_B/k_B)H\). \(H_{pg}\) (red squares) and \(T^*\) (blue triangles), obtained separately in the same crystals in the overdoped regimes, give a scaling \(g\mu_B H_{pg} \approx k_B T^*\) with \(g = 2.0\) (inset). Open and crossed symbols are from our analysis of \(\rho_c(H,T)\) in Refs. [31] and [32], respectively. The shaded band covers \(T^*(p)\) in cuprates [22] taken from Fig. 26 of Ref. [1].