Measurement of the Casimir force with a ferrule-top sensor

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Abstract. We present a Casimir force setup based on an all-optical ferrule-top sensor. We demonstrate that the instrument can be used to measure the gradient of the Casimir force between a gold-coated sphere and a gold-coated plate with results that are comparable to those achieved by similar atomic force microscope experiments. Thanks to the monolithic design of the force sensor (which does not require any optical triangulation readout) and to the absence of electronics on the sensing head, the instrument represents a significant step forward for future studies of the Casimir effect under engineered conditions, where the intervening medium or the environmental conditions might be unsuitable for the use of more standard setups.

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1. Introduction

Long-range surface interactions are of paramount importance in the design of micro- and nanoelectromechanical systems (MEMS and NEMS), as they determine the minimum separation that two miniaturized mechanical pieces can reach before they snap to contact. It is thus not surprising that, over the last decade, an ever increasing number of groups have been drawing the attention of the scientific community to the potential relevance of the Casimir effect in nanotechnology [1, 2] and what currently goes under the name of quantum fluctuations engineering—the possibility of tailoring the Casimir force with a suitable choice of the shape and material properties of the interacting objects and the medium between them [3]–[10]. Driven by this trend, scientists have developed a wide variety of instruments that can assess different aspects of this interaction mechanism. Macroscopic setups [13]–[16] and micromachined torsional balances [17]–[19] are typically optimized for utilization in a vacuum or air, but would hardly work in liquids. Experiments in a vacuum can also be performed by means of custom-made atomic force microscopes (AFMs) [20, 21], which, after proper modification, can be also used to measure the Casimir force in gaseous environments [8] or in liquids [7]. Because AFMs rely on optical triangulation, however, it is difficult to imagine a universal measuring head that can easily adapt to different environments, ranging, for example, from low-temperature vacuum to room temperature liquids.

Earlier this year, our group proposed overcoming this issue by replacing the AFM head with an all-optical micromachined torsional force sensor that adapts well to both vacuum and critical environments [22]. The sensor is based on fiber-top technology [23]. It consists of a mechanical rectangular beam carved out of the cleaved end of a standard single mode optical fiber. The beam is suspended a few microns above the rest of the fiber by means of two lateral torsional rods. The light coupled from the opposite end of the fiber allows one to measure the tilting angle of the rectangular beam and, therefore, the force that makes it tilt. Thanks to its monolithic design and the absence of electronics on the sensing element, this micro-opto-mechanical balance can in principle be used in any environment without any change of the readout mechanics, optics or electronics. Unfortunately, however, preliminary experiments show that, as soon as measurements are not carried out in a vacuum, the sensor can only be used in static mode [22]. Dynamic modes, which are typically more sensitive, are in fact disturbed by spurious effects induced by the hydrodynamic force between the mechanical beam and the fiber below (a phenomenon that goes under the name of squeezed field air damping [24]). Furthermore, because the optical fiber is only 125 µm in diameter, fiber-top devices are typically fabricated with an expensive and time-consuming technique (such as focused ion beam (FIB) milling [25]). Fiber-top technology cannot thus be considered as a practical solution for systematic measurements, where, due to recurrent accidental damaging of the force sensor, one must rely on probes that can be easily replaced.

To overcome the fabrication issue of fiber-top devices, we recently introduced a novel approach that preserves the flexibility of fiber-top technology while reducing manufacturing costs and production time: the ferrule-top cantilever [26]. To fabricate a ferrule-top cantilever,
a standard single-mode optical fiber is glued inside the bore hole of a much bigger pierced ferrule. The fiber and the ferrule are so well held together by the glue that they behave like a single mechanical piece. The ferruled fiber is thus equivalent to a very large single-mode optical fiber that can now be milled in the form of a cantilever by means of more convenient techniques (e.g. laser ablation). Interestingly, because of the larger dimensions of the building block, the gap between the cantilever and the remaining part of the ferrule is typically much larger than in fiber-top devices. Ferrule-top cantilevers are thus supposed to suffer considerably less from hydrodynamic problems than fiber-top sensors.

In this paper, we present a ferrule-top force setup designed to measure the Casimir attraction between a sphere and a flat plate, and we demonstrate that one can indeed perform precise measurements of the Casimir force between a sphere and a plate kept in air with a dynamic detection scheme that does not induce any spurious effects.

2. Experimental setup

The experimental setup presented in this paper is designed to measure the Casimir force between a 200 \(\mu\text{m}\) diameter sphere and a plate as a function of separation in a distance range between approximately 50 and 200 nm.

The force sensor is realized according to the scheme sketched in figure 1. A pierced 2.5 mm \(\times\) 2.5 mm \(\times\) 7 mm rectangular ferrule, made of borosilicate glass, is initially carved by means of laser ablation in the form of a cantilever that stretches over one of the diagonals of the edge of the ferrule. At the end of the milling process, a small amount of transparent epoxy is dropped and cured inside the 127 \(\mu\text{m}\) diameter hole left open at the center of the cantilever, while a standard single-mode optical fiber is slid into the hole of the ferrule from the other side and glued with the cleaved end at approximately 100 \(\mu\text{m}\) from the bottom surface of the cantilever. A 200 \(\mu\text{m}\) diameter sphere is then attached to the top of the free-hanging end of the sensor by means of a small droplet of UV curable epoxy. The sensor and the sphere are finally coated with a 5 nm thick Cr adhesion layer followed by a 200 nm thick Au film.

The ferrule-top device is anchored on top of a manual translation stage, just in front of a gold-coated sapphire plate that is attached to a piezoelectric stage (see figure 2). The manual manipulator allows a first coarse approach of the sensor towards the plate, while the piezoelectric stage is used for the actual scanning during the force-versus-distance measurements. The translational stage also hosts a bare cleaved optical fiber, parallel to the ferrule-top sensor, that is used to measure movements of the piezoelectric stage. The setup is fixed to a block of aluminum that is kept at a fixed temperature by means of four resistors controlled via a feedback circuit. To reduce acoustic and seismic coupling to the environment, the whole instrument is mounted on a silicone pad inside an anechoic chamber on top of a marble table equipped with passive vibration damping blocks.

To simultaneously measure the deflection of the ferrule-top cantilever and the motion of the piezoelectric stage, we built two fiber optic interferometers that are fed with the same laser source (Thorlabs Pro800 chassis with a WDM tunable laser module (1552.48–1554.18 nm)) (see figure 2). The laser light is split by a 50/50 optical fiber coupler into two forward branches. In both forward branches, the light is then split again by 90/10 couplers and sent toward the ferrule-top cantilever and the bare cleaved fiber. For the ferrule-top sensor, the light is reflected by the fiber-to-air, air-to-glue and glue-to-gold interfaces. The amount of light traveling...
Figure 1. Fabrication steps followed to manufacture a ferrule-top cantilever for Casimir force measurements. The building block is a pierced 2.5 mm × 2.5 mm × 7 mm rectangular ferrule made of borosilicate glass. The ferrule is machined in the form of a rectangular cantilever, which is then equipped with a spherical bead. An optical fiber slid through the central hole and glued to the ferrule allows the detection of cantilever deflections by means of interferometric techniques. The bottom figure is a composite of six scanning electron microscope images showing the device used in the experiment described in this paper.

backwards into the fiber is given by

\[ W(d_{\text{gap}}) = W_0 \left[ 1 + V \cos \left( \frac{4\pi d_{\text{gap}}}{\lambda} + \phi_0 \right) \right], \]

where \( d_{\text{gap}} \) is the distance between the fiber end and the cantilever, \( W_0 \) is the mid-point interference signal, \( V \) is the fringe visibility, \( \lambda \) is the laser wavelength and \( \phi_0 \) is a phase shift that only depends on the geometry of the cantilever [26]. This reflected light travels back into the fiber and is split again by the coupler, which sends part of the signal onto a photodetector (Thorlabs PDA10CS). Reading the current generated on the photodetector, which is proportional to \( W(d_{\text{gap}}) \), one can measure changes in \( d_{\text{gap}} \) (see equation (1)) and thus the external forces that have produced those changes. The other branch of the double interferometer works identically to the ferrule-top branch, except that the reflected signal is composed of reflections from the fiber-to-air interface and from the gold mirror, allowing one to measure the relative position of the piezoelectric stage.
Figure 2. Sketch of the experimental setup used to measure the Casimir force between a plate and a sphere attached to a ferrule-top cantilever. The ferrule-top cantilever is anchored to a translational stage that allows one to coarsely move the sensor with the sphere close to the plate. The plate is attached to a piezoelectric stage for fine-tuning the separation between the two interacting surfaces. A bare fiber is anchored parallel to the force sensor and is used to measure movements of the piezoelectric actuator via interferometric techniques. An electronic circuit supplies an ac voltage between the sphere and the plate, which allows one to compensate for the residual electrostatic force and calibrate the force sensor. The setup is mounted on an aluminum block kept at a fixed temperature inside an anechoic box and isolated from the surroundings with passive vibration dampers (not shown).

From equation (1), it is clear that it is convenient to operate the force sensor in its quadrature point, where the readout is most sensitive and linear in deflection [27]. For this reason, before each experiment, we first coarsely bring \( d_{\text{gap}} \) close to quadrature by adjusting the temperature set-point of the setup, which induces differential thermal expansions on the different parts of the ferrule-top device. We then use the tunable laser wavelength to precisely tune \( \lambda \) to the quadrature point\(^3\).

Casimir force measurements are carried out following a method similar to that described in [8, 28], which allows one to simultaneously calibrate the instrument, counterbias the

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\(^{3}\) The 1.7 nm wavelength variation spanned by our laser source alone is not always sufficient to adapt the laser wavelength to the actual length of the fiber-to-cantilever gap.
electrostatic potential difference that exists between the sphere and the plate and measure the
gradient of the Casimir force as a function of separation.

In a nutshell, while slowly changing the separation between the sphere and the plate by
means of the piezoelectric stage, we supply an ac voltage to the sphere with frequency \( \omega_1 \)
much smaller than the resonance frequency of the force sensor. This ac voltage gives rise to
an electrostatic force that makes the cantilever oscillate. The mechanical oscillation has one
component at \( \omega_1 \) and one component at \( 2\omega_1 \). The \( \omega_1 \) component drives a negative feedback loop
that compensates for the contact potential difference that exists between the sphere and the plate,
while the \( 2\omega_1 \) component allows one to calibrate the instrument and to measure the separation
between the interacting surfaces. On top of the electrostatic force modulation, we add a small
oscillatory motion to the piezoelectric stage at a frequency \( \omega_2 \) that lies somewhere between \( \omega_1 \)
and \( 2\omega_1 \). From the in-phase motion of the cantilever at \( \omega_2 \), we can finally measure the gradient
of the force between the sphere and the plate.

For details of the experimental method, see [8, 28]. It is, however, important to stress
that, contrary to the piezoelectric stage of the setup presented in [8, 28], the one used in this
experiment is driven via an open loop circuit and is not equipped with any internal calibration
sensor. For this reason, we have implemented a slightly different method to determine the
separation between the two surfaces. To explain this new approach, we first note that the
electrostatic force generated by the ac voltage is equal to

\[
F_e = \frac{\varepsilon_0 \pi (V_{ac} \cos(\omega_1 t) + V_0)^2}{d},
\]

where \( \varepsilon_0 \) is the permittivity of air, \( R \) is the radius of the sphere and \( V_0 \) is the residual potential
difference. Therefore, the mechanical oscillation induced by the electrostatic force on the force
sensor at \( 2\omega_1 \) gives rise to a \( 2\omega_1 \) signal on the photodiode of the interferometer that scales like
\( S_{2\omega_1} \propto V_{ac}^2/d \). The proportionality constant can be measured by looking at the output signal of
the bare fiber interferometer. We know in fact that, when the bare fiber interferometer signal has
moved through exactly one interference fringe, the plate has moved for exactly \( \lambda/2 \). Once the
proportionality constant \( \beta \) is known, one can extract \( d \) from

\[
d = \beta \cdot \frac{V_{ac}^2}{S_{2\omega_1}}.
\]

3. Results and discussion

The sensor used for the data presented below was a 3.4 mm long, 200 \( \mu \)m wide and 40 \( \mu \)m
thick ferrule-top cantilever (resulting in an expected spring constant of \( \approx 2 \text{ N m}^{-1} \)) with
\( \approx 100 \mu \text{m} \) ferrule-to-cantilever gap (see the scanning electron microscope image of figure 1).
The resonance frequency was measured independently, and resulted to be equal to 2.7 kHz, with
a \( Q \)-factor of 42.

In figures 3 and 4, we show the results of a typical measurement run. Data were gathered
during ten consecutive back-and-forth scans. Each scan had a duration of 1000 s and a stroke
of 1 \( \mu \)m spanned by applying a driving voltage to the piezoelectric stage of the form \( V_{YZT} \propto 1 - |t/\tau_s - 1|^3 \), with \( \tau_s = 500 \text{ s} \). The frequency of the ac voltage was set to \( \omega_1 = 72 \text{ Hz} \). Its
amplitude was continuously adjusted during the scan to keep the root mean square (rms) of the
\( 2\omega_1 \) electrostatic force component equal to roughly 230 pN at all separations (see [8, 28]). The
oscillation frequency of the piezoelectric stage was set to \( \omega_2 = 119 \text{ Hz} \) with 7.2 nm amplitude.
Signals at \( 2\omega_1 \) and \( \omega_2 \) were demodulated with two lock-in amplifiers equipped with a 24 dB
low-pass filter with RC time of 200 and 100 ms, respectively. To avoid mixing of the Casimir
signal with that induced by the hydrodynamic force due to the air in the gap [8], the phase of the \( \omega_2 \) lock-in amplifier was aligned with the phase of the oscillatory motion by going to contact, where the plate and the cantilever move synchronously. This procedure was performed only once before starting the measurement run.

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Figure 3 shows the potential difference $V_0$ needed to minimize the electrostatic interaction between the sphere and the plate as a function of separation $d$. The observed spread in the data is due to measurement noise and not to a time-related drift. It is clear that the data loosely follow a behavior like $a \log d + b$, as observed before in [14, 28] and [29]. This dependence is not yet fully understood.

Figure 4 shows the Casimir force gradient as a function of separation. The data were obtained by subtracting from the original data an electrostatic contribution that arises from the calibration procedure [8]. This contribution, which scales like $1/d$, can be accurately calculated from the value of $S_{2\omega_1}$. In our experiment, this correction ranged from $15 \text{N m}^{-2}$ at $200 \text{nm}$ to $70 \text{N m}^{-2}$ at $45 \text{nm}$. The gray line in the graph represents the theoretical Casimir force as computed from the Lifshitz equation, where we have assumed that the dielectric function of the gold surfaces can be obtained by combining the tabulated data of [30] with the Drude term described in [31] and where we have neglected surface roughness corrections. The theoretical result should thus not be taken too rigorously. It is known, in fact, that gold layers deposited with different methods may have different optical properties, which can lead to significant differences in the resulting Casimir force [32]. Furthermore, surface roughness corrections can be as high as several tens of per cent at the closest separations. A more refined calculation of the expected force is, however, beyond our scope. The goal of this paper, in fact, is not to improve the accuracy in the comparison between theory and experiment, but to prove that ferrule-top cantilevers can be successfully used to obtain precise (i.e. low noise, small statistical error in force gradient) Casimir force measurements.

It is thus now important to discuss the statistical error in the Casimir force gradient. The inset of figure 4 shows a histogram of the residuals of all the Casimir force data collected in the separation range between 160 and 200 nm. The standard deviation is equal to $2.5 \text{N m}^{-2}$. For comparison, our state-of-the-art AFM for Casimir force measurements is currently capable of achieving a standard deviation of $1.75 \text{N m}^{-2}$ [33] with an $\omega_2$ oscillation amplitude a factor of 2 lower but an integration time ten times higher.

4. Conclusions

We have presented a ferrule-top sensor for Casimir force experiments. The sensor is based on a monolithic miniaturized cantilever that is coupled to a remote readout via optical fibers. We have demonstrated that the setup provides measurements of the Casimir force between a sphere and a plate by means of a dynamic detection scheme. The sensor can be easily fabricated with cost-effective techniques, allowing frequent substitution of the probe in systematic experiments. Furthermore, it adapts well for utilization in harsh environments, such as low temperatures, vacuum and liquids. Similar ferrule-top devices can of course be used to investigate other long-range interaction mechanisms as well. Ferrule-top technology can thus be considered as a new tool for exploring phenomena that are of relevance in the future development of MEMS and NEMS.

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