Simulations of galaxy formation with radiative transfer: hydrogen reionization and radiative feedback

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ABSTRACT

We carry out hydrodynamical simulations of galaxy formation that simultaneously follow radiative transfer of hydrogen-ionizing photons, based on the optically thin variable Eddington tensor approximation as implemented in the \textsc{gadget} code. We consider only star-forming galaxies as sources and examine to what extent they can yield a reasonable reionization history and thermal state of the intergalactic medium at redshifts around \( z \sim 3 \). This serves as an important benchmark for our self-consistent methodology to simulate galaxy formation and reionization, and for future improvements through accounting of other sources and other wavelength ranges. We find that star formation alone is sufficient for reionizing the Universe by redshift \( z \sim 6 \). For a suitable choice of the escape fraction and the heating efficiency, our models are approximately able to account at the same time for the one-point function and the power spectrum of the Lyman \( \alpha \) forest. The radiation field has an important impact on the star formation rate density in our simulations and significantly lowers the gaseous and stellar fractions in low-mass dark matter haloes. Our results thus directly demonstrate the importance of radiative feedback for galaxy formation. The spatial and temporal importance of this effect can be studied accurately with the modelling technique explored here, allowing more faithful simulations of galaxy formation.

Key words: galaxies: formation – intergalactic medium.

1 INTRODUCTION

In the standard cosmological model, the primordial gas recombines and becomes neutral around redshift \( z \sim 1000 \). However, the absence of Gunn–Peterson troughs in the spectra of high-redshift quasars up to \( z \leq 6 \) (White et al. 2003; Fan et al. 2006) suggests that hydrogen is highly ionized at low redshift. Thus, there must be a period in the history of the Universe when hydrogen became ionized again, but it is still an open question when the process of this cosmic reionization started, how it proceeded in detail and which sources of radiation were primarily responsible for it.

An important observational clue about reionization is provided by the total electron-scattering optical depth to the last scattering surface of the cosmic microwave background (CMB), found to be \( \tau_{\text{es}} = 0.08785 \pm 0.00072 \) by the latest \textit{Wilkinson Microwave Anisotropy Probe 7} (WMAP7) data release (Larson et al. 2010). This points to an early start and possibly extended period of reionization. Further observational information about the history of hydrogen reionization can be inferred through different astrophysical phenomena. The Gunn–Peterson troughs in quasar spectra are sensitive to small trace amounts of neutral hydrogen during the late stages of reionization (\( z \sim 6 \)); Lyman \( \alpha \) emitting galaxies probe the intermediate stages of reionization (\( 7 < z < 15 \)); the 21-cm line background and gamma-ray bursts (GRBs) probe the early stages of reionization, when the Universe was mostly neutral (\( 10 < z < 30 \)); and finally, the CMB polarisation provides important data on the free electron column density integrated over a large range of redshifts (Alvarez et al. 2006). In the future, upcoming observations from new radio telescopes such as Low Frequency Array (LOFAR) promise to be able to map out the epoch of cosmic reionization in unprecedented detail, making theoretical studies of this process especially timely.

Population III stars are commonly believed to be the first significant sources of photons for reionization. They are very massive, short-lived stars and form around redshift \( z \sim 30 \), or even earlier (Gao et al. 2007). Another, in principle plausible candidate for causing reionization, are quasars. Madau, Haardt & Rees (1999) compare luminosity and spacial density functions of quasars and star-forming galaxies and show that quasars alone are unlikely to be the dominant sources of photons for reionizing the Universe. On the other hand, other groups (Trac & Gnedin 2009; Thomas et al. 2009)
predict in recent work that quasars can produce enough ionizing photons to be able to reionize the Universe. In many scenarios, reionization is assumed to be driven mainly by high-mass objects with mass $M > 10^6 M_\odot$ (Ciardi et al. 2000). However, the dim but abundant low-mass sources ($M < 10^4 M_\odot$) may still strongly influence the way in which the ionized regions grow (Sokasian et al. 2003; Choudhury & Ferrara 2007). These small galaxies are preferentially found in low-density environments along the cosmic web and may contain many metal-free Population III stars in the early Universe. It has been estimated that these low-mass haloes account for about 80 per cent of the total ionizing power at $z \sim 7$ (Choudhury & Ferrara 2007). Disregarding them may lead to an overestimate of the number of photons required to reionize the Universe (Sokasian et al. 2003).

Numerous theoretical studies have begun to investigate in detail the characteristic scales and the topology of the reionization process through the use of numerical simulations (e.g. Gnedin & Ostriker 1997; Gnedin 2000; Miralda-Escudé, Haehnelt & Rees 2000; Gnedin & Abel 2001; Sokasian, Abel & Hernquist 2001; Ciardi, Stoehr & White 2003; Sokasian et al. 2004; Iliev et al. 2006b; Zahn et al. 2007; Croft & Altay 2008; Shin, Trac & Cen 2008; Wise & Abel 2008). However, due to the high computational cost and complexity of the radiative transfer (RT) problem, most simulations, with very few exceptions (Gnedin & Ostriker 1997; Kohler, Gnedin & Hamilton 2007; Shin et al. 2008; Wise & Abel 2008), have treated reionization through post-processing applied to static or separately evolved gas density fields. This neglects the fact that the radiation field may exert important feedback effects on galaxy formation itself (e.g. Iliev, Shapiro & Raga 2005; Yoshida et al. 2007; Croft & Altay 2008). It is therefore an important task to develop more accurate theoretical models based on self-consistent simulations where the ionization field is evolved simultaneously with the growth of cosmic structures, a topic that we address in this work.

In the literature, predictions based on simulations for the onset of reionization range from redshifts $z \sim 30–40$ (Iliev et al. 2009; Wise & Abel 2008) to $z \sim 15–20$ (Norman, Paschos & Abel 1998; Abel, Bryan & Norman 2002). Reionization then probably proceeds in an inhomogeneous and patchy fashion (Iliev et al. 2009; Lidz et al. 2007), reflecting the inhomogeneous density distribution of the large-scale structure. At first, many isolated ionized bubbles are formed. They then grow in size from $\sim 1$ Mpc during the early stages of reionization up to $> 10$ Mpc in the late phases (Furlanetto, McQuinn & Hernquist 2006; Iliev et al. 2006b). Around redshift $z \sim 13$ (Iliev et al. 2006b), $8 < z < 10$ (Lee et al. 2008), or $z \sim 6$ (Gnedin & Fan 2006), the ionized regions overlap. These values are very uncertain and depend strongly on the modelling details of reionization and the parameters of the underlying galaxy formation simulations. However, it is plausible that the future use of more self-consistent simulation techniques should be able to reduce the systematic modelling uncertainties.

In this work, we therefore use the new RT algorithm we developed in a previous study (Petkova & Springel 2009) to carry out high-resolution simulations of cosmic structure growth in the proper cosmological context. The approximation to RT employed, the optically thin variable Eddington tensor approach (Gnedin & Abel 2001), is fast enough to allow coupled radiative-hydrodynamic simulations of the galaxy formation process. At the same time, the employed moment-based approximation to the RT problem can be expected to be still reasonably accurate for the reionization problem. In particular, thanks to the photon-conserving character of our implementation of RT and of the chemical network, ionization fronts are bound to propagate with the right speed. The Lagrangian smoothed particle hydrodynamics (SPH) we use automatically adapts to the large dynamic range in density developing in the galaxy formation problem. Combined with the fully adaptive gravitational force solver implemented in GADGET, this yields a numerical scheme that is particularly well suited for the cosmic structure formation problem.

For a first assessment of our new approach, we study simulations of the standard $\Lambda$ cold dark matter ($\Lambda$CDM) cosmology and treat star formation and supernova feedback with the interstellar medium (ISM) sub-resolution model developed in Springel & Hernquist (2003a). For simplicity, we shall here only consider ordinary star-formation regions as sources of ionizing radiation. We are especially interested in whether the star formation predicted by the simulations results in a plausible reionization history of the Universe, and whether it at the same time yields a thermal and ionization state of the intergalactic medium (IGM) at intermediate redshifts that is consistent with that probed by observations of the Lyman $\alpha$ forest. Finally, we are interested in possible differences induced in galaxy formation due to the spatially varying radiative feedback in the RT simulations, especially in comparison with the much simpler and so far widely adopted treatment where a spatially homogeneous UV background is externally imposed.

This paper is structured as follows. We start in Section 2 with a brief summary of our methods for simulating hydrogen reionization. We then present our results in Section 3, focusing on the history of reionization in Section 3.1, the Lyman $\alpha$ forest in Section 3.2 and the feedback from reionization in Section 3.3. We end with a discussion and our conclusions in Section 4.

2 SIMULATING HYDROGEN REIONIZATION

2.1 Radiative transfer modelling

For our work we use an updated version of the cosmological simulation code GADGET (Springel, Yoshida & White 2001; Springel 2005), combined with the RT implementation of Petkova & Springel (2009). The RT equation is solved using a moment-based approach similar to the one proposed by Gnedin & Abel (2001). The resulting partial differential equation essentially describes an anisotropic diffusion of the photon density field $n_\gamma$,\footnote{Differently from Petkova & Springel (2009) we solve equation (1) for the photon density $n_\gamma$, rather than the photon overdensity, with respect to the hydrogen density $\bar{n}_\gamma = n_\gamma/\bar{n}_H$.}

$$\frac{\partial n_\gamma}{\partial t} = c \frac{\partial}{\partial x_j} \left( \frac{1}{\kappa} \frac{\partial n_\gamma H_{ij}}{\partial x_j} \right) - c \kappa n_\gamma + s_\gamma,$$

(1)

where $c$ is the speed of light, $\kappa$ is the absorption coefficient, $H_{ij}$ is the Eddington tensor and $s_\gamma$ is the source function. The closure relation for this particular moment-based method is obtained by approximating the Eddington tensor $H_{ij}$ as

$$H_{ij} = \frac{P_{ij}}{\text{Tr}(P)}$$

(2)

where $P_{ij}$ is the radiation pressure tensor

$$P_{ij}(x) \propto \int \dd^3x' \rho_\gamma(x') \frac{(x-x')(x-x')_i (x-x')_j}{(x-x')^4}.$$  

(3)

This estimate of the Eddington tensors is carried out in the optically thin regime, giving the method its name.
The abundances of hydrogen and helium species are updated by accounting for the processes of photoionization, collisional ionization and recombination:

\[
\frac{\partial \tilde{n}_\text{H}^+}{\partial t} = \gamma_{\text{H}} \tilde{n}_\text{He} n_\text{H} + c \sigma_e \tilde{n}_\text{He} \tilde{n}_\text{H} - \alpha_{\text{H}} \tilde{n}_\text{H} n_\text{H},
\]

(4)

\[
\frac{\partial \tilde{n}_\text{He}^+}{\partial t} = \gamma_{\text{He}} \tilde{n}_\text{He} n_\text{H} - \gamma_{\text{He}} \tilde{n}_\text{He} \tilde{n}_\text{H}
\]

(5)

\[+ \alpha_{\text{He}} \tilde{n}_\text{He} n_\text{H} \]

(6)

\[
\frac{\partial \tilde{n}_\text{He}^0}{\partial t} = \gamma_{\text{He}} \tilde{n}_\text{He} n_\text{H} - \alpha_{\text{He}} \tilde{n}_\text{He} n_\text{H},
\]

(7)

where all abundances of hydrogen species (\(\tilde{n}_\text{H}^+\), \(\tilde{n}_\text{H}^0\)) are expressed in dimensionless form relative to the total number density \(n_\text{H}\) of hydrogen, all helium abundances are fractions with respect to the helium number density, and the electron abundance is expressed as \(\tilde{n}_e = n_e / n_\text{H}\). Furthermore, \(\gamma\) denotes the collisional ionization coefficient, \(\epsilon\) is the recombination coefficient and \(\sigma_0 = 6.3 \times 10^{-15} \text{ cm}^2\) is the photoionization cross-section for hydrogen at 13.6 eV. These rate equations are solved using a semi-implicit scheme.

The photo-heating of the gas by the ionizing part of the spectrum is described by the heating rate

\[
\Gamma = n_\text{H} \int_0^\infty \frac{4 \pi l_\nu}{h \nu} \sigma_e (h \nu - h_\nu)
\]

(8)

\[= n_\text{H} c n_\nu \tilde{\epsilon}_\text{H}, \]

(9)

where

\[
\tilde{\epsilon} = \int_0^\infty \frac{4 \pi l_\nu}{h \nu} \sigma_e \left( \int_0^\infty \frac{4 \pi l_\nu}{h \nu} \right)^{-1}
\]

(10)

is a frequency-averaged photoionization cross-section and

\[
\tilde{\epsilon} = \int_0^\infty \frac{4 \pi l_\nu}{h \nu} \sigma_e (h \nu - h_\nu) \left( \int_0^\infty \frac{4 \pi l_\nu}{h \nu} \sigma_e \right)^{-1}
\]

(11)

is a frequency-averaged photon excess energy (Spitzer 1998). For our calculations, we usually assume a blackbody spectrum with \(T_{\text{eff}} = 10^4 \text{ K}\), which leads to \(\tilde{\epsilon}_\text{H} = 1.63 \times 10^{-18} \text{ cm}^3\) and \(\tilde{\epsilon}_\text{H} = 6.4 \text{ eV}\). However, given the uncertainties in accurately calculating the net energy input during the photoionization transition, which involves non-equilibrium processes, we will later on vary \(\tilde{\epsilon}_\text{H}\) in order to investigate the influence of different heating efficiencies.

We have tested our RT implementation on the static cosmological density field that was used in the RT code comparison study by Iliev et al. (2006a). In Fig. 1 we show the ionized fraction in a slice through the simulated volume at evolution time \(t = 0.05 \text{ Myr}\). Reassuringly, our result is in good agreement with the ones obtained by other radiative codes in the comparison study.

### 2.2 Treatment of star formation and radiative cooling

We follow the radiative cooling of helium and hydrogen with a non-equilibrium treatment, with the rates as cited in Petkova & Springel (2009). Winds and star formation in the dense, cold gas are modelled in a sub-resolution fashion (Springel & Hernquist 2003a), where the ISM is pictured as being composed of cold clouds that are embedded at pressure equilibrium in a hot tenuous phase that is heated by supernova explosions. Through the evaporation of clouds, this establishes a tight self-regulation of the star formation rate (SFR). Previous work has shown that this model converges well with numerical solutions and yields SFRs that are consistent in the Kennicutt relation (Kennicutt 1998) observed at low redshift. We shall here assume that the same star formation law also holds at high redshift.

We use the star-forming regions in all simulated galaxies as sources of ionizing photons in our RT model. We adopt an ionizing source luminosity of \(N_{\text{SFR}} = 10^{31} \text{ photon M}_{\odot}^{-1} \text{ yr}^{-1}\) (Madau et al. 1999), which relates the number of emitted photons to the SFR in units of \(\text{M}_{\odot} \text{ yr}^{-1}\). This source luminosity is released individually by every star-forming gas particle, hence the number of numerically represented sources is a non-negligible fraction of all simulation particles. Fortunately, the speed of our RT algorithm is almost insensitive to the total number of sources, because the Eddington tensor calculation can be carried out with a tree algorithm similar to the gravity calculation. This insensitivity of the computational cost to the number of sources is a significant advantage of the method used here, and is not shared by most alternatives for treating RT.

To account for the uncertain absorption that occurs in reality in the spatially unresolved multiphase structure of our simulations, we impose a phenomenological efficiency factor \(\eta\) on the source luminosities. In our simulation set, we explore values in the range \(\eta = 0.1–1.0\) to get a feeling for the sensitivity of our results to this uncertainty. We note however that \(\eta\) should not be confused with what is usually called galaxy escape fraction, which has a slightly different meaning. Our \(\eta\) is meant to be just an ‘ISM escape fraction’ whereas photon losses in the gaseous haloes of galaxies will be taken into account self-consistently in our simulations.

### 2.3 Simulation set

All our simulations assume a \(\Lambda\)CDM universe with cosmological parameters \(\Omega_0 = 0.27, \Omega_\Lambda = 0.73, \Omega_\gamma = 0.044, h = 0.7\) and \(\sigma_8 = 0.9\). In order to have sufficiently high mass resolution, we follow a comparatively small region in a periodic box of comoving size \(L_{\text{box}} = 10 h^{-1} \text{ Mpc}\) on a side. This region is still sufficiently large to give a representative account of the Lyman \(\alpha\) forest at redshift \(z = 3\), which is the final time of our runs.

Our primary simulation set has \(2 \times 128^3\) dark matter (DM) and gas particles, giving a mass resolution of \(3.04 \times 10^7\) and \(5.29 \times 10^8 h^{-1} \text{ M}_{\odot}\) in DM and gas, respectively. A selected model was also carried out at the much higher resolution of \(2 \times 256^3\), giving a gas...
mass resolution of $6.62 \times 10^7 \, h^{-1} \, M_\odot$. The gravitational softening was chosen as $1/35$ of the mean particle spacing in each case, corresponding to $\epsilon = 2.23$ and $1.12 \, h^{-1} \, \text{kpc}$ in the two resolution sets. In order to save computational time, most runs were restarted from $z = 20$ with different RT treatments, such that the higher redshift evolution did not have to be repeated. We have also systematically varied the ‘escape fraction’ $\eta$ and the heating efficiency $\epsilon$, considering the values $\eta = 0.1, 0.2, 0.3, 0.5, 1.0$ and $\epsilon = 6.4, 16, 20, 30 \, \text{eV}$ for the low resolution set. For the high resolution run, we chose the parameters $\eta = 0.2$ and $\epsilon = 30 \, \text{eV}$. In this way we could systematically determine the settings that give the most promising agreement with the observations.

3 RESULTS

3.1 Hydrogen reionization history

When star formation starts at around redshift $z = 20$ in our simulations, the process of reionization begins through photoionization of the gas around the star-formation sites. However, as the dense gas has a high recombination rate, the progress in the reionization is sensitively determined by a competition between the luminosity of the sources, the rate with which they turn on and the density of the neutral gas they are embedded in. Using our simulation set, we first investigate the global reionization history and its dependence on the source efficiency parameter $\eta$.

Fig. 2 shows the reionization histories of our low resolution simulated box for several choices of $\eta$. As expected, the results for the reionization redshift depend strongly on $\eta$. For larger efficiencies, the Universe gets reionized earlier, since more photons become available to ionize the hydrogen. This effect always overwhelms the reduction in star formation and hence source luminosity that an increased efficiency parameter $\eta$ also induces. In all cases the last phase of the Epoch of Reionization (EoR) is rather short, i.e. the final 10 per cent of the volume transition very rapidly from being neutral to being essentially fully ionized. The redshift of reionization when this occurs varies between $z \sim 5$ and 8 for $\eta = 0.1$ and 1.0, respectively. In contrast, the EoR starts in general at much higher redshift. For example, the highest efficiency $\eta = 1.0$ model has already ionized nearly 30 per cent of the volume by redshift $z = 10$. Interestingly, there is a systematic variation of the time it takes to complete the last phase of the EoR. This is much more rapid for the high efficiency model than for the lower efficiency ones. Since typical bubble sizes at redshift $z = 6$ are up to $10 \, h^{-1} \, \text{Mpc}$, we note that the size of our simulation box is really too small to draw any definitive conclusions about the global duration of reionization in the Universe. A number of authors (Ciardi et al. 2003; Furlanetto & Oh 2005; Furlanetto & Mesinger 2009) have pointed out that the local reionization history depends on the environment, so that, for example, the evolution of the neutral fraction in a field or void region is different than in a protocluster region. As a result, only very large simulation volumes of $100 \, h^{-1} \, \text{Mpc}$ or more on a side can be expected to yield a truly representative account of cosmic reionization. Since at the same time an equal or better mass resolution as we use here is required, such calculations are very expensive and beyond the scope of this work, but should become feasible in the future on the next generation of high-performance computers.

In Fig. 3 we compare the ionizing background for the same simulations, which gives further interesting clues about the reionization histories of the different models. The background is computed as the volume-averaged intensity in the simulation box. The ionizing background is compared with an analytical estimate by Haardt & Madau (1996) for the metagalactic ionizing flux from quasars rather than stellar sources, which is an interesting comparison point for the expected value of the background. Clearly, lowering the efficiency $\eta$ decreases the ionizing background as well, consistent with the findings above. Interestingly, the rapid rise of the

Figure 2. Volume-averaged neutral fraction as a function of redshift for the low-resolution simulations. The different colours represent simulation results for different values of the efficiency parameter (or ‘ISM escape fraction’) $\eta = 0.1, 0.2, 0.3, 0.5, 1.0$. Reionization happens earlier for higher efficiency since then more photons become available for ionizing the gas. In all cases, the final phase of reionization proceeds rapidly; over a small range of redshift, the neutral volume fraction drops from 10 per cent to negligibly small values.

Figure 3. Ionizing background for the low-resolution simulation as a function of redshift for different efficiency $\eta = 0.1, 0.2, 0.3, 0.5, 1.0$. As expected, the background becomes higher for a larger efficiency since more of the photons emitted by the sources are made available to build up the ionizing background. The thin solid line shows the background computed by Haardt & Madau (1996) for quasars, which provides for an interesting comparison. Our results for the time evolution of the neutral volume fraction agree quite well with previous studies (e.g. Gnedin 2000).
mean background intensity ends when reionization is complete. From this point on, the background shows only a weak residual evolution.

The time evolution of the temperature, ionized fraction and density fields in a representative simulation model ($\eta = 0.1$ and $\bar{\epsilon} = 30 \text{ eV}$) is illustrated in Fig. 4. The different panels correspond to slices through the middle of the simulation box, between redshifts $z = 7.2$ and 4, from the top row to the bottom row. It is seen that the ionized regions start to grow first around high-density peaks, where the star-forming regions are concentrated. Then the radiation diffuses into the intercluster medium. The filaments remain less ionized than the voids for a while, since their density is much higher. Initially the photons heat up the gas in the ionized region to temperatures slightly above $10^4 \text{ K}$. As the ionizing background declines due to the expansion of the Universe and the drop of star formation, the heating becomes less effective and the temperature of the highly ionized gas in the voids drops somewhat as a result of the expansion cooling.

In Fig. 5, we present a contour plot of the neutral fraction versus the overdensity of the gas in the representative model for two different redshifts, at $z = 6.4$ before reionization is completed, and at $z = 3$ after reionization is completed. There is a clear dependence of the neutral fraction on overdensity in both cases. The high-density regions around star-forming matter are ionized very quickly. The average-density regions, e.g. filaments, tend to be less ionized and get ionized after the low-density regions. However, note that in the star-forming tale of the diagram all the gas is ionized. This is here due to the star formation scheme adopted in GADGET, where star-forming gas particles are assigned a mean mass-weighted temperature which is so high that all this gas is formally collisionally ionized. We note that these results are very similar to the ones reported by Gnedin (2000), where a similar relation between neutral fraction and density is found. However, we are able to probe somewhat higher densities, thanks to better spatial resolution of our simulations.

### 3.2 Lyman $\alpha$ forest

We next turn to an analysis of the thermal state of the IGM left behind at $z = 3$ by our self-consistent reionization simulations. To this end we use the gas density, gas temperature, gas velocity and ionization state of the gas in the simulation box and compute Lyman $\alpha$ absorption spectra for random lines of sight. We then compare the statistics of these artificial absorption spectra with observational data on the Lyman $\alpha$ forest at this epoch, as given by McDonald et al. (2000) and Kim et al. (2007). Here we assume that the main source of ionizing sources is stellar and thus discard any contribution from a quasar-type spectra, in agreement with Madau et al. (1999). We also note that some discrepancies are possible due to the fact that helium is not photoionized in our simulations, but only collisionally ionized.

Our simulations have the necessary gas mass resolution at redshift $z = 3$ required to reproduce realistic Lyman $\alpha$ absorption in the low-density regions (Bolton & Becker 2009). However, we cannot match the required simulation volume of size $\sim 40 h^{-1} \text{ Mpc}$ to properly sample the largest voids. This can have a significant effect on our predictions of the Lyman $\alpha$ flux probability distribution and power spectra. Fig. 6 shows the flux probability distribution function (PDF) and flux power spectrum for our simulation model, where an efficiency parameter of $\eta = 0.2$ and averaged photon excess energy $\bar{\epsilon} = 6.4 \text{ eV}$ were adopted. For this choice, we achieve the best fit to the flux PDF.

However, for all the other models, the power spectrum is overpredicted at high wave numbers. We suggest that this overestimation of the power spectrum is due to the insufficient heating of the gas in low-density regions, causing an excess of small-scale structure in the Lyman $\alpha$ forest.

In order to examine this effect further, we vary the photon excess energy $\bar{\epsilon}$ used in the photo-heating and examine the influence this has on the flux probability and power spectrum. There are two possible reasons why our simulations underestimate the photo-heating. First, we expect that some non-equilibrium effects in the photo-heating are treated inaccurately due to our implicit treatment of the radiation transport and chemistry (e.g. Bolton & Becker 2009). Secondly, photo-heating is different in optically thin and optically thick regions. For example, in an optically thick region the average photon excess energy obtained from equation (11) is $\bar{\epsilon} = 29.9 \text{ eV}$. It is however likely that our approximative RT scheme leads to inaccuracies in the effective heating rates of regions of different optical depths, due to the varying accuracy of the scheme in different regimes. Part of these inaccuracies can be absorbed into a suitably modified value of the effective heating rate $\bar{\epsilon}$. To explore the full range of plausible values, we therefore vary the values for $\bar{\epsilon}$ as follows: $\bar{\epsilon} = 6.4, 16, 20$ and 30 eV. We aim to bracket what can be expected when non-equilibrium effects are fully taken into account in future treatments, and want to identify the case that provides the best representation of the Universe at redshift $z = 3$.

Fig. 7 shows the flux PDF and power spectra for these different heating values. Clearly, the high wave number region of the flux power spectrum is strongly influenced by the amount of injected heat energy into the gas, and the increase of the temperature also affects the flux probability distribution. For the low efficiency of $\eta = 0.1$, there is a substantial mismatch already in the flux PDF, simply because there is too little ionization overall so that the mean transmission ends up being too low. However, as the adopted photo-heating energy increases, the gas is getting hotter and is able to stay ionized longer due to the higher temperatures, yielding a better fit to the flux PDF. At the same time, small-scale structure in the flux power spectrum is erased due to thermal broadening, bringing the simulations into agreement with the observation. This shows the power of detailed Lyman $\alpha$ data to constrain simulations of the reionization process. In our current models, we need to adopt a quite extreme heating efficiency of $30 \text{ eV}$ combined with a low ‘escape fraction’ of $\eta = 0.1$ to achieve a good match to the data.

In Figs 8 and 9 we compare the impact of the different photo-heating efficiencies on the evolution of the neutral volume fraction and the ionizing background. We also show for comparison the results from our high resolution simulation, which is discussed below in the text. As expected, an increase in the heating energy leads to a slightly earlier reionization and to a slightly elevated ionizing background flux. Both of these effects can be readily understood from the higher gas temperature produced in the ionized gas when the higher heating efficiency is adopted. However, the effect is quite weak, and very much smaller than the changes resulting from a different choice of $\eta$.

We also measured the Thomson electron scattering optical depth in our high-resolution simulation and found it to be $\tau_{\text{es}} = 0.049$, which is smaller than the WMAP7 value $\tau_{\text{WMAP}} = 0.088 \pm 0.015$ (Komatsu et al. 2010). This discrepancy is, however, not critical since the simulated volume is too small to obtain a realistic value and we have also not included photoionization of helium.

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Figure 4. Slices through the middle of the simulated volume for the low-resolution simulation realization with $\eta = 0.1$ and $\tilde{\zeta} = 30$ eV. The maps are showing the density (left) with contours at ionized fraction $\tilde{n}_{\text{H}} = 0.001, 0.5$ and 0.9 overlaid, ionized fraction (middle), and temperature (right) of the gas. The snapshots show a time evolution from top to bottom, with individual redshifts $z = 7.2, 6.4, 5.7, 5$ and 4, respectively.
Simulations of galaxy formation with RT

3.3 Feedback from reionization

Reionization can in principle exert a strong feedback effect on the gas through the temperature increase induced by photo-heating. As the gas temperature increases, the gas densities will be lowered through pressure effects. The gas will then cool and collapse more slowly, such that the SFR is ultimately reduced. Especially small DM haloes should be sensitive to this effect. In the extreme case of haloes that have virial temperatures comparable to or only slightly larger than the temperature reached by the gas through reionization, the UV radiation may even completely suppress atomic cooling and efficient star formation. This effect is often invoked to explain why so many of the DM satellites expected in $\Lambda$CDM in the haloes of ordinary $L_\star$ galaxies are apparently largely devoid of stars.

In order to highlight the RT effects on the star formation in galaxies, we compare our simulations with two fiducial models where no RT is used. The first is a simulation simply without any photo-heating of the gas, while the second one is a simulation where reionization is induced by an externally imposed, spatially homogeneous UV background based on a modified Haardt & Madau (1996) model that causes reionization and an associated photo-heating of the gas at $z = 6$ (for details see Davé et al. 1999). The latter model corresponds to the standard approach applied in many previous hydrodynamical simulation models of galaxy formation (e.g. Tornatore et al. 2003; Wadepuhl & Springel 2010).

In Fig. 10, we compare our results for the cosmic SFR density evolution as a function of the adopted efficiency parameter $\eta$ (for the low-resolution simulation set). We also include the two fiducial comparison models as limiting cases. As we increase the escape efficiency of the ionizing radiation, the star formation drops, as expected, since this makes more photons available to photo-heat the gas. We note that our results for the SFR are always lower than the fiducial simulation where no photo-heating is included at all, consistent with findings by Pawlik & Schaye (2009). Towards lower redshift, the reduction of the SFR due to the radiation field becomes progressively larger. The run with $\eta = 0.2$ quite closely corresponds to the simulation with the imposed reionization epoch, but starts to slightly differ at redshifts $z < 4$. 

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Figure 5. Scatter plot of the neutral fraction as a function of overdensity for two different redshift of the low-resolution simulation realization with $\eta = 0.1$ and $\tilde{\epsilon} = 30$ eV. The thick dashed line is the median neutral fraction. The neutral fraction shows a clear dependence with density, where high-density regions are more ionized than low-density regions. Very high-density gas is highly ionized as well, because it is in the star-forming stage.

Figure 6. Lyman $\alpha$ flux probability (left) and power spectrum (right) from the low resolution simulation with $\eta = 0.2$ and $\tilde{\epsilon} = 6.4$ eV at redshift $z = 3$. The result is compared with observational data from McDonald et al. (2000) and Kim et al. (2007). The flux probability agrees reasonably well with observations, whereas the power spectrum deviates at the high $k$ end. We discuss this problem in the text.

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Figure 7. Lyman $\alpha$ flux probability (left) and power spectrum (right) for the low-resolution simulation with efficiency $\eta = 0.1$, for four different values of the averaged excess photon energy $\tilde{\epsilon} = 6.4, 16, 20, 30$ eV. The simulated data are compared to the observational result from McDonald et al. (2000) and Kim et al. (2007).

We also carry out a corresponding comparison for a low-resolution simulation set with constant efficiency $\eta = 0.1$ but different values for the photon excess energy. In Fig. 11 we show the results for the SFR, again including the two fiducial models as limiting cases for comparison. The results confirm the expectation that an increase of the photon excess energy decreases the SFR density. Interestingly, the model that best reproduced the Lyman $\alpha$ power spectrum observations, the one with $\tilde{\epsilon} = 30$ eV, quite
Simulations of galaxy formation with RT

Figure 8. Volume-averaged neutral fraction as a function of redshift. The set of low-resolution simulations with efficiency $\eta = 0.1$ and average photon excess energy $\bar{\epsilon} = 6.4, 16, 20, 30$ eV is compared with the high-resolution run with $\eta = 0.2$ and $\bar{\epsilon} = 30$ eV. When a higher energy per ionizing event is injected, the universe gets ionized slightly earlier since higher temperatures help to maintain higher ionized fractions.

Figure 9. Ionizing background as a function of redshift. The set of low-resolution simulations with efficiency $\eta = 0.1$ and averaged photon excess energy $\bar{\epsilon} = 6.4, 16, 20, 30$ eV is compared with the high-resolution run with $\eta = 0.2$ and $\bar{\epsilon} = 30$ eV. For a higher injected energy per ionization event, the background also increases as a result of the higher temperature, which leaves more photons unabsorbed so that they can contribute to a higher level of the ionizing background.

Figure 10. SFR density as a function of redshift for the low-resolution simulation set at different efficiencies of $\eta = 0.1, 0.2, 0.3, 0.5, 1.0$. The results are compared to the SFR history of a low-resolution simulation with instantaneous reionization at $z = 6$ and photo-heating by a Haardt & Madau (1996) ionizing background (thin black line), and a simulation with neither reionization nor photo-heating (thick black line). The photo-heating from stellar sources decreases star formation, as suggested by Pawlik & Schaye (2009). As the escape efficiency gets higher, this effect becomes progressively stronger.

They are in good agreement, except for the higher redshift, where the high resolution captures more star formation, as expected (Springel & Hernquist 2003b). The Lyman $\alpha$ forest flux probability and power spectrum at $z = 3$ for this simulation are shown in Fig. 12. While the simulated data are in reasonable qualitative agreement with the observational results from McDonald et al. (2000) and Kim et al. (2007), it does not provide in this case a detailed fit within the error bars, again highlighting that simultaneously accounting for the cosmic star formation history, cosmic reionization and the state of the IGM at intermediate redshifts provides a powerful constraint on self-consistent simulations of galaxy formation and reionization.

In Fig. 13, we explore the temperature evolution of the gas at different characteristic densities, corresponding to underdense gas by a factor of 10, gas at the mean density and overdense gas by a factor of 10 relative to the mean. We compare our default simulation with RT and photo-heating to the fiducial simulation where no such heating is included at all. Clearly, the effect of photo-heating is most prominent in the lowest density gas. This gas is only weakly heated by structure formation shock waves when photo-heating is not included. In contrast, when reionization is accounted for, the temperature of this gas reaches a high value of $\sim 10^4$ K at the end of the epoch of cosmic reionization, and even before that, the mean temperature of this gas is raised considerably as a result of the patchy and temporally extended reionization transition in our RT simulations. Interestingly, after reionization is complete, the mean temperature of the underdense gas starts to slowly decline again, while already for the mean density gas structure formation shocks can provide for a slow further increase of the temperature.

We also analysed the median temperature of the gas as a function of overdensity. As shown in Fig. 14, after reionization has been completed, the low-density gas ends up with a higher median temperature than the higher density gas (except for the gas in the

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Figure 11. SFR density as a function of redshift. The set of low-resolution simulations with efficiency $\eta = 0.1$ and averaged photon excess energy $\bar{\epsilon} = 6.4, 16, 20, 30 \text{ eV}$ are compared to the high-resolution run with $\eta = 0.2$ and $\bar{\epsilon} = 30 \text{ eV}$. The results are compared to the SFR history of a low-resolution simulation with instantaneous reionization at $z = 6$ and photo-heating by a Haardt & Madau (1996) ionizing background (thin black line), and a simulation with neither reionization nor photo-heating (thick black line). The star formation decreases with increasing heating energy, as expected. For the low-resolution run with 30 eV, the result of the self-consistent RT calculation matches the simulation with instantaneous reionization. The high-resolution simulation SFR is higher at higher redshift due to better resolution and agrees well with the other results at redshifts less than $z = 6$.

star-forming phase). This points towards an ‘inverted equation of state’, as observed by Bolton et al. (2008), Trac, Cen & Loeb (2008) and Furlanetto & Oh (2009). At later times, the equation of state reverts again to a normal positive slope, when the low-density gas cools down due to the adiabatic expansion of the Universe.

Finally, in Figs 15, 16 and 17 we explore the impact of the ionizing radiation field on the gas and stellar mass content of individual DM haloes. To this end we run a group finder on our simulations and simply determine the average gas mass, stellar mass and baryon fraction of haloes as a function of their DM mass. We compare the $z = 3$ results of our higher resolution RT simulation with the simulation where photo-heating is completely ignored. Interestingly, we find a reduction of the gas and stellar mass for all halo masses when $\text{RT}$ is included. The effect is quite weak for large haloes but becomes progressively larger for small haloes. At DM halo masses of $M_{\text{DM}} = 10^9 \text{ M}_\odot$ the suppression in baryonic content is approximately 60 per cent, while at $M_{\text{DM}} = 10^{12} \text{ M}_\odot$ it drops to only a few per cent. This shows clearly the important impact of the ionizing radiation field on small dwarf galaxies, in particular. While an externally imposed UV background can perhaps account for the mean effect of this radiative feedback process (Hoef et al. 2006; Okamoto, Gao & Theuns 2008), only a spatially resolved treatment of RT can account for effects of proximity that may well play an important role in shaping, e.g. the satellite luminosity function (Muñoz et al. 2009; Busha et al. 2010; Iliev et al. 2010).

4 DISCUSSION AND CONCLUSIONS

We have presented the first application of our new implementation (Petkova & Springel 2009) of radiation hydrodynamics in the cosmological simulation code GADGET. We focused on the problem of cosmic reionization, aiming in particular at a first test on whether...
Figure 14. Median temperature of the gas as a function of overdensities \( \log_{10}(1 + \delta) \) at redshifts \( z = 5.09 \) and 3 for the high-resolution simulation with \( \eta = 0.2 \) and \( \bar{\epsilon} = 30 \) eV. At redshift \( z = 5.09 \), shortly after reionization is completed, the temperature at low densities is clearly higher than that at higher densities (apart from the gas in the star-forming phase). This can be interpreted as an inverted equation of state. At lower redshift, the relation reverts again to normal form as the gas in the low-density regions cools down adiabatically due to the expansion of the Universe.

Figure 15. Mean stellar and gas masses as a function of the DM halo mass at \( z = 3 \) in the high-resolution simulation. The black vertical corresponds to a mass of 100 DM particles, which can be taken as an (optimistic) resolution limit of the simulation. Photo-heating slows down the collapse of gas in haloes, which in turn also decreases their stellar and gas masses. The effect becomes stronger for low-mass DM haloes.

Figure 16. Baryon fraction as a function of the DM halo mass at \( z = 3 \) in the higher resolution simulation. The black vertical corresponds to a mass of 100 DM particles.

Figure 17. Baryon fraction as a function of DM halo mass at \( z = 3 \) in the lower resolution simulations with efficiency \( \eta = 0.1 \), and for different averaged photon excess energy. The dashed line shows the baryon fraction when no photo-heating has taken place. The black vertical line corresponds to a mass of 100 DM particles. Photo-heating does not affect the baryon fraction as strongly as in the high-resolution simulation. We also observe that differences in the excess photon energy do not have a large effect on the baryon fraction alone. Based on the encouraging results collected here, it is clearly worthwhile to extend the model further in future work.

Since the level of internal absorption in the ISM is uncertain and cannot be resolved by our simulations, we have examined models with different effective source efficiencies \( \eta \). Likewise, as we have not included a detailed spectral treatment and the time evolution of non-equilibrium in the chemistry may be inaccurate, we have parametrized the heat input per ionization event in terms of a parameter \( \bar{\epsilon} \).
We find that our simulated universes can get reionized by star formation in ordinary galaxies alone, with the epoch of reionization ending between redshifts $z = 8$ and 5, depending on the assumed escape efficiency. The final phase transition is always quite rapid in our setup, but sizable fractions of the volume begin to be reionized much earlier. The heating efficiency has only a weak influence on the reionization history, but a stronger one on the cosmic SFR density. In fact, we have shown that photo-heating plays an important role in the evolution of the baryonic gas. As a result of the associated heating, it changes baryonic structure formation by slowing down the collapse of gas in DM haloes, thereby delaying star formation. This effect is strongest for the lowest mass haloes, where the DM potential well is not deep enough to easily overcome the thermal pressure from the effects of photoionization.

Our simple models of a self-consistent treatment of galaxy formation and RT are not only able to produce a plausible history of reionization, but they also manage to approximately match the basic statistics of the Lyman $\alpha$ forest, at least for an appropriate choice of the parameters $\eta$ and $\bar{\epsilon}$. This suggests that the low-redshift IGM data can be a powerful additional constraint on future reionization modelling in structure formation simulations.

Despite these encouraging results, it is also clear that our simulation results are likely still affected by numerical resolution effects, because the resolution in the lowest mass haloes is still too coarse to yield fully converged results. Ideally, we would like to resolve the full range of star-forming haloes with enough particles to achieve fully converged results. While this is unlikely to qualitatively change any of the results presented here, future precision work will require such calculations. Another important caveat that will require further study are uncertainties due to the RT approximation itself. This is probably best addressed by comparing the results with a completely different approach to RT. We are presently finalizing such a scheme in the moving-mesh code AREPO. It avoids the use of the diffusion approximation and can cast sharp shadows, hence a direct one-to-one comparison with the optically thin variable Eddington tensor approach applied here will be particularly interesting.

ACKNOWLEDGMENTS

The authors would like to thank Benedetta Ciardi for the helpful discussion and comments. This research was supported by the DFG cluster of excellence ‘Origin and Structure of the Universe’ (www.universe-cluster.de).

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