Basics of particle therapy II: relative biological effectiveness

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In the previous review, the physical aspect of heavy particles, with a focus on the carbon beam was introduced. Particle beam therapy has many potential advantages for cancer treatment without increasing severe side effects in normal tissue, these kinds of radiation have different biologic characteristics and have advantages over using conventional photon beam radiation during treatment. The relative biological effectiveness (RBE) is used for many biological, clinical endpoints among different radiation types and is the only convenient way to transfer the clinical experience in radiotherapy with photons to another type of radiation therapy. However, the RBE varies dependent on the energy of the beam, the fractionation, cell types, oxygenation status, and the biological endpoint studied. Thus this review describes the concerns about RBE related to particle beam to increase interests of the Korean radiation oncologists’ society.

Keywords: Carbon, Proton, Particle beam therapy, Relative biological effectiveness

Introduction

Particle beam therapy can offer advantages of biological and physical dose distributions over conventional photon beam therapy. There are potential benefits in the use of particle beam therapy for treating anatomically complex and radioresistant malignant tumors because this therapy does not cause severe side effects in normal tissue [1]. Until today, there has been little interest in particle beam therapy in Korea, especially the use of heavy ion radiobiology. Thus we have described the radiobiology issues related to heavy ion beams in order to increase the interests by the Korean radiation oncologists’ society.

A characteristic of photons is a random energy distribution through the media in which the resultant ionization density is homogenous over the entire treatment volume. However, the photon beams generate relatively low ionization levels and many photons are required to achieve relevant therapeutic goals. The particle beams, especially heavy ion beams, provide a different characteristic in the spatial distribution of energy. The track structure produces a radial dose distribution around the ion path, which has 2 steps: the emission of electrons by Coulomb interaction and scatter of the emitted electrons [2]. Indirect DNA damage is found greater in low linear energy transfer (LET) radiation but high LET radiation such as carbon ions, creates greater direct hits [3].
The ionization process is composed of quasifree electrons, Auger electron and convoy electron. Subsequently, these electrons transfer energy by elastic and inelastic collisions. The ionization cross section of the electrons in water exhibits its maximum at approximately 100 eV, which relates to a mean free path of a few nanometers [2]. These electrons that are fast enough to leave the track core (\( \delta \) rays) typically undergo a large number of interactions. Due to those frequent scattering processes, the initial preference of electrons in the forward direction diminishes, resulting in a broad angle of distribution. These different energy distributions of heavy ions with a high local dose is on the order of nanometers resulting in a larger probability of correlated nearby DNA damages, such as single or double strand breaks and base damage.

For heavy ions, the dependence of relative biological effectiveness (RBE) on the various physical and biological properties is greater and cannot be disregarded. But this problem was solved by a number of pragmatic steps and assumptions, the clinical RBE is replaced by an LET-dependent RBE for in vitro data and well-defined conditions and then linked to clinical data by an empirical factor [4]. At clinical institutions, proton therapy is based on the use of an RBE value of 1.1 to 1.2, while for the heavier carbon ions the RBE distribution in the target volume varies between 2 and 5 [5].

1. Basic understandings about survival curves

Poisson statistics: In order explain theoretical models, a basic understanding of statistical derivatives is needed. The basic principle to calculate probability is derived in Poisson statistics. The probability of \( n \) event \( P(n) \) is given by:

\[
P(n) = \frac{(e^{-x})(x^n)}{n!}
\]

where \( x \) is the average number of events, \( n \) is the specific number of events and \( e \) is Euler’s number expressed as:

\[
e = \lim_{n \to \infty} \left(1 + \frac{1}{n}\right)^n \approx 2.71828
\]

If the probability of being hit is assumed as a kill or inactivation, the probability of not being hit \( P(0) \) is based on the following Poisson relationship

\[
P(0) = \frac{(e^{-x})(1^0)}{0!} = e^{-1} = 0.3679 \approx 37\%
\]

where \( x = 1 \), and \( n = 0 \).

Equations 4 to 11 of this section are based on the article “From DNA radiation damage to cell death: theoretical approaches” by Ballarini [6] published in Journal of Nucleic Acid 2010, which is an open access article permits unrestricted use, distribution, and reproduction in any medium, provided the original work is properly cited. The target model, which was first developed in 1946 and revised in 1955 [7], had limitations that they made no assumption about the induction and repair of the initial DNA damage; this is now known to play a fundamental role in radiation-induced clonogenic death. Therefore, the linear-quadratic (LQ) model has been adopted as the model of choice to describe survival curves (Fig. 1) [8]. In 1973, Chadwick and Leenhouts [9] developed a molecular model, which is now known as the LQ model.

Fig. 1. Linear quadratic survival curve after single dose irradiation. The \( \alpha \)-component represents non-repairable damage, while the \( \beta \)-component represents repairable damage. The damage caused by the \( \beta \)-component is repairable with time, so lowering the fractional dose results in lowering \( \beta \)-component damage to make \( \alpha/\beta \) increase. Theoretically, a very low dose rate (dose/time) radiation resembles \( \alpha \) curve. The \( \alpha/\beta \) can be plotted when the equation \( (\beta D^2 - \alpha DV_D) = 0 \) intersects the x-axis. RBE, relative biological effectiveness; LET, linear energy transfer.
If \( N_0 \) is the number of DNA molecular bond (target), \( N \) is the number of the bonds that remain intact after dose \( D \), and \( K \) is the damage probability of a single bond per unit dose, then

\[
-\frac{dN}{dD} = KN, \quad N = N_0 e^{-KD}
\]  

(4)

The number of effective damage (broken bond) is therefore

\[
N_0 - N = f N_0 (1 - e^{-KD})
\]  

(5)

Where \( f \) is the fraction of broken bonds and that are not repaired.

The double helix can undergo a double stands break (DSB) as the result of 2 different mechanisms: (i) both DNA strands are broken by the same radiation track (or event); (ii) each strand is broke independently, but the breaks are close enough in time and space to lead to a DSB. Let \( \Delta \) be the fraction of dose acting through mechanism (i), and \( 1-\Delta \) the fraction of dose acting through mechanisms (ii). The number of unrepaired DSBs per cell produced by mechanism (ii) is then

\[
Q_{II} = Ef_0 q_1 q_2
\]  

(6)

Where \( E \) is the “effective factor”; that is the likelihood for a DSB to occur from the 2 single stand breaks (SSBs) associated in time and space, \( f_0 \) is the fraction of unrepaired DSBs, and \( q_1 \) and \( q_2 \) are the number of broken bonds on strand 1 and 2, respectively. Therefore,

\[
q_1 = f_1 n_1 (1 - e^{-k(1-\Delta)D})
\]

\[
q_2 = f_2 n_2 (1 - e^{-k(1-\Delta)D})
\]  

(7)

Where \( n_1 \) and \( n_2 \) are the number of critical bonds on strand 1 and 2, respectively, \( f_1 \) and \( f_2 \) are the fractions of unrestored bonds in strand 1 and 2, and \( k \) is the probability of bond rupture per bond and per unit dose.

Adopting a similar notation, the number of unrepaired DSBs induced via mechanism (i) is

\[
Q_i = n_0 f_0 [1 - \exp (-k_0 \Delta D)]
\]  

(8)

Where \( n_0 \) is the number of DNA sites that can sustain a DSB and \( k_0 \) is the hit probability constant.

The average number of DSBs per cell is therefore \( Q_i + Q_{II} \), and the average number of lethal DSBs per cell is

\[
Q = p(Q_i + Q_{II})
\]  

(9)

Where \( p \) is the assumed proportionality constant between the DSB yield and cell death.

Lumping constant,

\[
Q = p[\varphi (1 - e^{-kD}) + \varphi (1 - e^{-k(1-\Delta)D})^2]
\]  

(10)

According to Poisson-type cell killing the probability of cell survival \( S \) is given by the probability of having 0 lethal lesions, \( S = e^0 \). Assuming that \( k \) and \( k_0 \) are quite small, the result is the familiar linear quadratic relationship as follows:

\[
S = \exp(-aD-\beta D^2)
\]  

(11)

where \( a = (f_0 E n_0 n_2 f_1 n_1 f_2 k_1^2 (1-\Delta)^2) \) and \( \beta = (f_0 E n_1 n_2 f_1 n_1 f_2 k_1^2 (1-\Delta)^2) \).

By this model, the expression for the survival curves can be drawn as \( S = e^{-(aD+\beta D^2)} \), and \( S \) is the fraction of cells surviving a dose \( D \). The constants \( a \) is used for the component proportional to dose \( (aD) \) and \( \beta \) is for the component proportional to the square of the dose \( (\beta D^2) \). Survival of the \( n \) fractions of dose size \( d \) is expressed as \( S = e^{-(ad+\beta d^2)} \). The \( a \)-component represents non-repairable damage, while the \( \beta \)-component represents repairable damage. The damage caused by \( \beta \)-component is repairable with time, so lowering the fractional dose results lowering \( \beta \)-component damage to increase \( a/\beta \). Theoretically, a very low dose rate (dose/time) radiation resembles an \( a \) curve.

The final slope of the survival curves of low LET and high LET radiation are similar, while the initial slopes are much different and show that densely ionizing radiation has a high \( a \)-component; the \( \beta \)-component remains unchanged [10]. Thus, irradiation of cells with high LET radiation levels produces linear survival curves. Then, for the high LET radiation, the relationship between the surviving fraction \( S \) and the dose \( D \) is:

\[
S = e^{-aD}
\]  

(12)

In the Fig. 1, the relationship between \( D_0 \) and \( a \) is expressed as \( D_0 = 1/a \) because survival after \( D_0 \) is \( e^{-1} \) therefore:

\[
S = e^{-D/D_0}
\]  

(13)

when \( D = D_0 \)
\[ S = e^{-1} = 0.3679 \approx 37\% \quad (14) \]

For this reason, the probability of not being hit \( P(0) \) in Poisson statistics can be compared, internally with \( D_0 \) in survival curves, which is often called the mean lethal dose, or the dose that delivers one lethal event per target.

**Relative Radiobiological Effectiveness**

The relative biological effectiveness is used to compare biological effectiveness among different types of radiation. In 1990, the International Commission on Radiological Protection (ICRP) advised the use of a weighting factor \( (W) \) of 1 for low LET radiations by ICRP-60 recommendations \[11\]. Later on, the ICRP accepted that in *in vitro* experiments on cells show significant differences in radiation quality between low LET radiations, but the ICRP continues to recommend a \( W(p) \) of 1 for all low LET radiations \[12\]. For the high LET radiations, the RBE is used to extrapolate the clinical experiences accumulated from the low LET radiation with the relevant radiation weighting factors. In order to transfer the experiences from photon therapy to particle beam therapy, the RBE is introduced as:

\[
\text{RBE} = \frac{D_{\text{photon}}}{D_{\text{particle}}} \quad (15)
\]

\( D_{\text{photon}} \) and \( D_{\text{particle}} \) are absorbed doses for photon and particle radiation, which lead to the same biological effect, respectively. The biologically effective dose of a photon or particle irradiation is then provided as the product of the absorbed dose multiplied by the RBE. Although it looks simple, the RBE varies with many factors (i.e., LET, energy, particle type, cell type, biological endpoint). These factors cause a serious limitation of the RBE usefulness. Nevertheless, RBE is used because it is the only convenient way to transfer the clinical experience of photon therapy to other types of radiation therapy. The unit of the biological effective dose, which is the Gray-equivalent (GyE) or Cobalt gray equivalent (CGE), if \(^{60}\text{Co} \) radiation is used as reference-beam quality. However, the use of these units is not encouraged by the International Commission on Radiation Units & Measurements - International Atomic Energy Agency (ICRU-IAEA) Task Group, where they recommended the sole use of the term, isoeffective dose, and of the unit, Gy.

The biologic properties of particle beams may differ from those of photons for which the biologic mechanisms have been highly investigated. While the radiobiologic properties of protons are thought to be similar to the photon, the neutrons or heavier ions may produce secondary protons, alpha particles, and heavier nuclear fragments that result in little or no repair of sublethal damage. Therefore, the use of particle therapy has some biological uncertainties that complicate its clinical application. Thus, a fundamental question arises: can the biological effect transferred from photons be used as the biological effect of the particle beam?, without any reductions in tumor control and/or increase in damage to normal tissue. At the end of 2009, a total of 78,275 patients were treated with particle therapy, and most of whom had been treated with proton therapy (67,079) followed by carbon therapy (7,151) \[13\]. Currently, most proton therapy centers use a generic RBE value of 1.1 in proton treatment planning \[14\], as recommended by the ICRU \[15\]. The use of generic RBE means the use of the same RBE in all positions in spread out Bragg peak (SOBP), at all dose levels per fraction and in all tissues. However, application of a single RBE value for protons is complicated because the RBE varies dependent on the energy of the proton \[16\], the fractionation \[17\], tissue types \[18\], oxygenation status \[19\], and the biological endpoint studied. Though it is widely accepted, a generic RBE cannot be a universal RBE for each tissue or dose/fraction. This is a special concern for young patients who might have secondary malignancy in the future \[20\]. The RBE can be used for many biological and clinical endpoints derived from DNA strand breaks to tumor cell killing. However, in the scope of particle beam therapy the RBE for cell killing and normal tissue complications are most relevant. Thus the authors discuss the concern about the RBE of particle beams.

**Factors Influencing Carbon Beam RBE**

1. **RBE of *in vivo* tumor model**

As previously described, the RBE depends on dose level and fractionation. RBE is high in lower dose and lower in large dose due to shoulder of photon survival curves \[21\]. In general, the biological differences between conventional radiation and particle beams are reported to be diminished if the dose is escalated. However, the RBE for clinical situations involves rather large uncertainties, RBEs for each tumor and normal tissues should be calculated for each instance. Thus RBE calculations using biological systems to evaluate RBE relationships at various depths and their dependence on dose per fraction are needed. Unfortunately, the studies addressing
carbon ion effects in vivo tumor models are relatively small and their endpoints are diverse [22-24]. A recent report for the RBE of carbon ion beams for local tumor control using a syngeneic rat prostate tumor model by Peschke et al. [25] is remarkable. In the report, they set the endpoints of ‘no tumor recurrence within 300 days’ and volumetric changes after irradiation. With single and split doses of either 12C ions or photons using a 20-mm SOBP the values for D10 were used to determine RBE values. A total of 198 rats were irradiated with single and split doses of either photons or carbon ions using a series of increasing dose levels ranging from 30 to 100 Gy for photon and 9 to 50 Gy for carbon. The RBEs for the endpoint were 2.30 ± 0.08 for single fraction and 2.38 ± 0.16 for two fractions. The experiment showed that there was only a very small fractionation effect for both beam qualities. The D10 isoeffect ratio of 1.20 for 2 vs. 1 fraction of photons is not markedly different from that of 1.16 for carbon ions. The reports suggest that the RBE of any reference point should be calculated independently for each clinical application.

2. RBE and LET
In the tissue exposed to heavy ions, the RBE is low in the entrance at high energy and increases at the end of the particle range [26]. As the higher ionization density in the track center of particles with a larger LET, the radiation damage became more severe, and thus increasing the RBE. RBE increases with LET up to an ion-dependent maximum value and decreases for higher LET values [27]. It has been reported that the RBE increases as a function of LET up to a maximum value which, for high Z high energy (HZE) charged particles, is found at LET values between 100 and 250 keV/μm [28]. Koike et al. [24] reported RBEs in animal tumor models using NFSa fibrosarcoma model in mice with different LET. In this study, a clear relationship between RBE and LET was documented. They treated fractionated doses of 290 MeV/u carbon ions. With LET of 14 and 20 keV/μm, RBEs were 1.4 and independent of the number of fractions, whereas those for 44 and 74 keV/μm, the RBE was increased from 1.8 to 2.3 and from 2.4 to 3.0, respectively, when the number of fractions changed from 1 to 4. Raising the number of fractions from 4 to 6 was not associated with a further increase in RBE. In another report, Suzuki et al. [29] irradiated sixteen different human cell lines with carbon beam of two different LET values. They calculated RBE values by the D10 which is determined as the dose required to reduce the surviving fraction to 10%, relative to X-rays. The calculated RBE ranged from 1.06 to 1.33 for 13-keV/microm-beam and from 2.00 to 3.01 for approximate 77-keV/microm-beam irradiation on each cell line. There was a good correlation in the D10 values of each cell line between X-rays and carbon-ion beams and the cellular radiosensitivity of different cell lines well correlated among different types of radiation. Notably, two normal cell lines were included in the experiments, suggesting there was no trend for a higher RBE for tumor than normal cell lines. However, the clinical experience with neutron therapy, which is a representative high LET radiation, showed a high RBE for late responding normal tissues (low α/β) evidenced by the increased frequency of late complications. Thus a carbon irradiation would be predicted to be more effective against slowly growing and low α/β tumors, vide infra [30].

3. RBE and cell type
RBE varies with the nature of cellular characteristics. Weyrather et al. [21] irradiated three hamster cell lines of differing repair capacity with monoenergetic carbon ions. RBE values for cell inactivation at different survival levels were determined and the differences in the RBE-LET patterns were compared with the individual sensitivity. Three hamster cell lines, the wild-type cell lines V79 and Chinese hamster ovary (CHO)-K1 and the radiosensitive CHO mutant xrs5, were irradiated with carbon ions of LET values (13.7-482.7 keV/μm). For the repair-proficient cell lines a RBE maximum was found at LET values between 150 and 200 keV/μm. For the repair-deficient cell line the RBE failed to show a maximum and decreased continuously for LET values above 100 keV/μm. The carbon RBE-LET relationship for inactivation is shifted to higher LET values and the RBE correlated with the repair capacity of the cells. Belli et al. [31] irradiated two cancer cell lines and three normal tissue cell lines to compare RBE of monoenergetic carbon-ion beams (incident LET 13-303 keV/μm) with three dose-averaged LET values (40, 50, and 75 keV/μm). In the report, the data showed the superior effectiveness for cell-killing exhibited by carbon-ion beams compared to lower LET radiation, particularly in tumor cells radioresistant to X- or γ-rays, hence the advantage of using such beams in radiotherapy. These reports suggest that the variation of cellular nature may result in RBE changes for cell-killing that should be exploited before clinical application. From radiobiological studies, carbon beam treatment may show a high RBE for cell-killing in cells that are repair proficient and radioresistant to X- or γ-rays [32] but also may imply a greater risk in normal tissue for late effects than X- and γ-rays.
or protons [33]. Preclinical studies for interested normal or tumor cell lines are therefore fundamental for assessing these radiobiological properties of different cell and tissues.

4. RBE and particle type

In clinical setting, the carbon ions are much faster than protons resulting in broader tracks with a reduced ion density in the track center so that at the same LET range, the cell killing effect of carbon ions is smaller than protons. In order to achieve the maximum RBE for the carbon ion, slower ions velocity with a correspondingly smaller track size and higher LET are required. Likewise, for heavier particles, the RBE maximum is typically sifted to higher LETs. Because the LET sharply increases at the end of the particle’s path, forming the Bragg peak, whereas the shape of Bragg peak depends on the type of particles. However, when plotted against dose averaged LET, RBE distributed so widely that no relation between LET and RBE could be found except a trend showing large RBE at around 80-200 keV/mm [34]. George et al. [35] reported chromosome aberrations of human lymphocytes after in vitro exposure to $^1$H, $^3$He, $^{12}$C, $^{20}$Ne, $^{40}$Ar, $^{28}$Si, $^{56}$Fe, or $^{197}$Au ion beams, with LET ranging from approximately 0.4-1,393 keV/microm in the dose range of 0.075-3 Gy. In the report, the estimates of RBEmax values for mitotic spreads, which ranged from near 0.7 to 11.1 for total exchanges, increased with LET, reaching a maximum at about 150 keV/microm, and decreased with further increase in LET. Han et al. [36] investigated primary Syrian hamster embryo (SHE) cell transformation by silicon ions and carbon ions. In the report, the RBE for carbon ions ranged from 2.2 to 6.9 and for silicon ions ranged from 2.0 to 6.0. Czub et al. [37] compared RBE for cell inactivation and LET in the Bragg peak region of $^{12}$C and $^{20}$Ne ions. CHO-K1 cells were exposed to high LET $^{12}$C ions (33.2 MeV, 20.3 MeV, and 9.1 MeV at cell entrance) and $^{20}$Ne ions (56.2 MeV, 34.7 MeV, and 15 MeV at cell entrance) and to low LET x-rays. RBE has been measured for LET values close to the Bragg peak maximum, i.e., 440-830 keV/microm for $^{12}$C and for 1,020-1,600 keV/microm for $^{20}$Ne ions. The RBE decreases with increasing LET in the range between 440 and 1,600 keV/microm for the two types of radiations forming a single line when plotted together, pointing towards LET as the single determinant of RBE. These reports suggest that the RBE varies with particle type end biological endpoints, however, when they plotted against dose averaged LET, the RBE of heavy particles varies so widely that no clear relationship can be made between particle types and RBE.

RBE of Carbon Beam

1. Single fractionation

The RBE of high LET radiation is defined as the ratio of the tested high LET radiation dose to that required from low LET radiation to achieve that effect [10,38]. The following equations are modified from the equations of Dale et al. [38].

$$RBE = \frac{d_L}{d_H}$$ (16)

Where $d_L$ is dose of low LET and $d_H$ is dose of high LET radiation.

The survival of low LET radiation and high LET radiation are expressed as:

$$S_L = \exp (-\alpha_L d_L - \beta_L d_L^2)$$

$$S_H = \exp (-\alpha_H d_H - \beta_H d_H^2)$$ (17)

Thus the logarithms of the survival become

$$\ln S_L = -d_L (\alpha_L + \beta_L d_L)$$

$$\ln S_H = -d_H (\alpha_H + \beta_H d_H)$$ (18)

Then,

$$d_L = -\frac{\ln S_L}{(\alpha_L + \beta_L d_L)} , d_H = -\frac{\ln S_H}{(\alpha_H + \beta_H d_H)}$$ (19)

Then the RBE is expressed as:

$$RBE = \frac{\ln S_L}{(\alpha_L + \beta_L d_L)}\Big / \frac{\ln S_H}{(\alpha_H + \beta_H d_H)}$$ (20)

If the fractional dose get closer to 0 ($D \rightarrow 0$), In $S_L$ and In $S_H$ become 1 ($10^0$) and the $\beta$ contribution becomes minimal ($D \rightarrow 0$, $\beta \rightarrow 0$). It can be expressed as

$$RBE_{\beta \rightarrow 0} = \frac{\alpha_H}{\alpha_L}$$ (21)

If the fractional dose becomes large enough, the In $S_L$ becomes closer to In $S_H$ and $\alpha$ contribution becomes minimal ($D \rightarrow \infty$, $\alpha \rightarrow 0$). Thus it can be expressed as:

$$\beta_L d_L^2 = \beta_H d_H^2$$ (22)
According to LQ model, RBE is maximal when dose $\rightarrow 0$. If the fractional dose becomes large enough, the $\ln S_I$ becomes closer to $\ln S_H$ and $\alpha$ contribution becomes minimal ($D \rightarrow \infty, \alpha \rightarrow 0$). According to linear quadratic model, RBE is maximal when dose $\rightarrow 0$. If the fractional dose increases, the RBE converges to a minimal value.

$$d_l^2 = \frac{\beta_H}{\beta_L}$$

$$RBE_{\alpha \rightarrow 0} = \frac{\beta_H}{\beta_L}$$

According to LQ model, RBE is maximal when dose $\rightarrow 0$. At this point the $\alpha$-component occupies the most effective component of the biologic effect. If the fractional dose increases, the RBE converges to a minimal value. $RBE_{\beta \rightarrow 0}$ is $RBE_{\text{max}}$ and $RBE_{\alpha \rightarrow 0}$ is $RBE_{\text{min}}$ (Fig. 2). This suggests that the difference between the RBEs is reduced with larger doses per fraction. However, larger fractional dose is related to an increase in complications.

$$RBE_{d \rightarrow 0} = RBE_{\text{max}} = \frac{\alpha_H}{\alpha_L}$$

$$\alpha_H = \alpha_L RBE_{\text{max}}$$

With the concept that the RBE means the same biological effect in both low LET and high LET radiation, $\ln S_I = \ln S_H$.

Thus,

$$\alpha_L D_L + \beta_L D_L^2 = \alpha_L RBE_{\text{max}} D_H + \beta_H D_H^2$$

$$\alpha_L RBE_{\text{max}} D_H = (\alpha_L D_L + \beta_L D_L^2) - \beta_H D_H^2$$

$$RBE_{\text{max}} = \frac{\alpha_L D_L + \beta_L D_L^2 - \beta_H D_H^2}{\alpha_L D_H}$$

When dose $\rightarrow 0$, the $\beta$ contribution goes to negligible level and we can assume $\beta_H = \beta_L$.

$$RBE_{\text{max}} = \frac{(\alpha_L D_L + \beta_L D_L^2) - \beta_H D_H^2}{\alpha_L D_H}$$

$$RBE_{\text{max}} = \frac{\alpha_L (\alpha_L D_L + \beta_L D_L^2) - \beta_H D_H^2}{\alpha_L D_H}$$

From equation 27,

$$(\alpha_L D_L) / D_H + (\beta_L D_L^2) / D_H =$$

$$(\alpha_L RBE_{\text{max}} D_H) / D_H + (\beta_H D_H^2) / D_H$$

$$(\alpha_L RBE_{\text{max}} D_H) / D_H = \alpha_L RBE_{\text{max}} + \beta_H D_H$$

$$\alpha_L RBE_{\text{max}} + \beta_H D_H$$

$$\alpha_L RBE_{\text{max}} = \alpha_L RBE_{\text{max}} + \beta_H D_H$$

$$\alpha_L RBE_{\text{max}} = \alpha_L RBE_{\text{max}} + \beta_H D_H$$

$$(\alpha_L RBE_{\text{max}} D_H) / D_H =$$

$$(\alpha_L RBE_{\text{max}} D_H) / D_H =$$

$$\alpha_L RBE_{\text{max}} = \alpha_L RBE_{\text{max}}$$

$$\alpha_L RBE_{\text{max}} = \alpha_L RBE_{\text{max}}$$

$$\alpha_L RBE_{\text{max}} = \alpha_L RBE_{\text{max}}$$

$$(\alpha_L + \beta_L D_L) RBE^2 = (\alpha_L RBE_{\text{max}} + \beta_H D_H) - \beta_H D_H = 0$$

$$RBE = \frac{\alpha_L RBE_{\text{max}} + (\alpha_L RBE_{\text{max}})^2 + 4 \alpha_L (\alpha_L + \beta_L D_L) (\beta_L D_L)}{2 \alpha_L (\alpha_L + \beta_L D_L)}$$

When dose $\rightarrow 0$, the $\beta$ contribution goes to negligible level and we can assume $\beta_H = \beta_L$.

$$RBE = \frac{\alpha_L RBE_{\text{max}} + (\alpha_L RBE_{\text{max}})^2 + 4 \alpha_L (\alpha_L + \beta_L D_L) (\beta_L D_L)}{2 \alpha_L (\alpha_L + \beta_L D_L)}$$

Divide with $\beta_L$.

$$RBE = \frac{(\alpha_L D_L + \beta_L D_L^2) - \beta_H D_H^2}{\alpha_L D_H}$$

$$RBE = \frac{(\alpha_L D_L + \beta_L D_L^2) - \beta_H D_H^2}{\alpha_L D_H}$$

2. Multiple fractionation

In 2008, Dasu and Toma-Dasu [39] reported a clinical relevant RBE model warning about fractionated therapy with high LET radiation. The reliability on the transfer of tolerance and curative levels from low LET radiation to high LET radiation by using RBE was questioned. They introduced the dose modifying factor (DMF) concept to simplify the formula (Fig. 3). The effects of high LET radiation can be described using similar...
equations, either by using different $\alpha$ and $\beta$ parameters or by applying DMF to the parameters describing the response to low LET radiation. DMF is drawn by experimental data.

A brief citing of their formula is that RBE means the ratio of the low LET dose to high LET dose with 'same biologic effect' so that it can be expressed as

$$ RBE = \frac{D_{HL}}{D_{HH}} $$

Thus RBE can be drawn by the factors of high LET radiation.

For the RBE of fractionated radiation, a similar approach can be used.

$$ n(\alpha d_L + \beta d_L^2) = n(\alpha D_{HL} + \beta D_{HL}^2) $$

$$ d_L(\alpha + \beta d_L) = d_H(\alpha D_{HL} + \beta D_{HL}^2) $$

$$ RBE_{FX} = \frac{D_{HL}}{D_{HH}} = \frac{-\alpha \pm \sqrt{\alpha^2 + 4\beta C}}{2\beta D_{HL}} $$

For details on the derivation of the above formula, further reading is recommended [39].

With this equation, the authors compared the RBE of single fractionation and multiple fractionations. The authors showed that the clinically relevant RBE increased for greater doses per fraction when multiple fractions were applied, in contrast to the predictions from single-dose experiments (Fig. 4). Furthermore, the RBE of late-reacting tissues appeared to modify more quickly than that for early-reacting tissues. The authors concluded that the modification of the RBE with dose per fraction must be carefully taken into consideration when devising fractionated treatments with high LET radiation. They also emphasized that neglecting to do so may result in an avalanche of complications that could obscure the potential advantages of the therapeutic use of this radiation type.

The RBE in SOBP may increase further. Karger et al. [40] compared the tolerance of the rat spinal cord to photon and carbon ion irradiations in the plateau region and in a 1-cm SOBP. Rats were irradiated with 6 or 18 fractions of photons...
or $^{12}$C-ions, respectively and followed up for 300 days for
the onset of paresis grade II and dose-response curves were
analyzed. The corresponding RBE-values were $1.33 \pm 0.02$
$1.42 \pm 0.02$ (6 and 18 fractions, $^{12}$C-plateau) and $2.97 \pm 0.05$
$5.04 \pm 0.08$ (6 and 18 fractions, $^{12}$C-peak), respectively. The
experiment showed that carbon ion irradiations of the spinal
cord are significantly more effective in the peak than in the
plateau region. In the Bragg-peak, it may underestimates the
RBE by 25%.

**RBE in Practice: HIMAC vs. GSI**

RBE itself is a simple concept expressed as $D_{\text{photon}}/D_{\text{carbon}}$.
But in clinical practice, very complicated extrapolations of
concerning factors are required for therapeutic planning
because it depends on many factors such as dose [21], LET [27],
particle type, and cell types [29]. The RBE differences between
conventional radiation and particle beams decreased if the
dose is escalated because RBE is high in lower dose and low
in large dose due to shoulder of photon survival curves [21].
The RBE varies with LET. RBE increases with LET up to an ion-
dependent maximum value and decreases at higher LET values
[27]. Due to the higher ionization density in the track center,
the LET in increased resulting more severe radiation damage,
thus the RBE is increased. However, as the LET increased
further, the number of ions required for the same dose become
relatively lower to make the hitting probability decreased (low
efficacy). Also, the RBE varies according to the characteristics
of tissue or cell type. Suzuki et al. [41] determined the survival
curves for more than a dozen lineages of normal and tumor
cells. In the report, the RBE values calculated by the $D_{\text{sp}}$
ranged from 1.06 to 1.33 for low LET radiation, and from 2.00 to 3.01
for high LET radiation. Another characteristic of radiation
sensitivity $\alpha/\beta$ ratio showed correlation with RBE, because RBE
depends on the $\alpha/\beta$ ratio after conventional photon irradiation
so that RBE increases with decreasing $\alpha/\beta$ ratio [42]. Therefore,
the RBE of carbon ions may relate to the $\alpha/\beta$ ratio determined
by photon. Considering these factors, an effort for clarification
and application of clinical RBE were made in the carbon
therapy facilities. However, their concepts on carbon RBE were
much different.

The heavy-ion medical accelerator complex (HIMAC), which
first started heavy ion therapy, used experimental data
combined with clinical neutron experience data. At first, they
calculated the depth dose distribution and LET distribution of
a monoenergetic carbon beam. *In vitro* survival experiments
using mono-energetic carbon ions were performed. Then a
dose weighted average based algorithm was set. Then relative
shape of depth dose distribution curve was made [29]. It was
found that the neutron RBE at several survival levels coincided
with the RBE of the carbon beam at a dose averaged LET
around 65 keV/μm. Thus they assumed that the neutron beam
is nearly equivalent to a 65 keV/μm carbon beam. As a next
step, a clinical neutron experience was combined to determine
absolute RBE [4]. As a result, a clinical carbon RBE at the center
of the SOBP was determined as 2.38 [4]. Finally, it was noticed
that the RBE for the inactivation of human salivary gland cells
of a carbon SOBP at the 80 keV/μm position coincides with the
RBE of a neutron beam. But this cellular RBE = 2 was much
smaller than the clinical neutron RBE = 3. Consequently, for
the clinical treatment planning of carbon beams the RBE at
the 80 keV/μm position was fixed to the neutron value RBE
= 3, independently from dose and fractionation schedule.
Currently, the National Institute of Radiological Sciences (NIRS)
is developing a model based on spot scanning system, which is
totally different from the passive scanning system that is used
first carbon therapy in HIMAC.

The Gesellschaft fur Schwerionenforschung (GSI) developed
their own biophysical model called local effect model (LEM).
The basic assumption of GSI model is that biological damage is
determined by local dose and there is no qualitative difference
since the damage is generated by ejected delta electrons. The
only difference is that local distribution of dose. The principle
of local effect model is:

Local biological effect $S$ is

$$ S = e^{-N_{\text{lethal}}} $$

(49)

Low LET dose response is

$$ N_{\text{lethal}}(D) = -\ln S_x(D) = \alpha D + \beta D^2 $$

(50)

The event density is

$$ v(D) = \frac{N_{\text{lethal}}(D)}{V_{\text{Nucleus}}} $$

(51)

So,

$$ N_{\text{lethal}} = \int \frac{-\ln S_x(d(x,y,z))}{V_{\text{Nucleus}}} dV_{\text{Nucleus}} $$

(52)

Currently the LEM III is reported where the description of
track structure is modified by taking into account a velocity-
dependent extension of the inner part of the track to improve the accuracy [42]. They reported that the original version of the LEM (LEM I) underestimates the therapeutic ratio of carbon ions (i.e., the ratio of RBE in the Bragg peak region as compared with the RBE in the entrance channel). Although significantly reduced, the cluster extension of the LEM (LEM II) still shows the same tendency. Implementation of the modified track structure (LEM III) almost completely compensates these systematic deviations, and predictions of RBE by LEM III for high and low energetic carbon ions show good agreement for a wide panel of different cell lines, as well as for the tolerance of the rat spinal cord. As a consequence, the expected RBE in the normal tissue surrounding the tumor becomes significantly lower than estimated with the LEM in its original version (LEM I). They concluded that LEM III model will be particularly useful for further optimization of carbon ion therapy in general.

Recently, the RBE of HIMAC model and GSI model were directly compared [43]. Even with the different concepts of two models and different methods for beam delivery of two institutes, the RBE difference was not big in the report. They compared biological effectiveness of 290 MeV/amu carbon-ion beams in Chiba, Japan and in Darmstadt, Germany. Murine small intestine and human salivary gland tumor (HSG) cells exponentially growing in vitro were irradiated with 6-cm width of SOBPs adjusted. Cobalt-60 gamma rays were used as the reference radiation. Isoeffective doses at given survivals were used for RBE calculations and inter-institutional comparisons. As a result, isoeffective D_{10} doses of HSG cells ranged from 2.37 ± 0.14 Gy to 3.47 ± 0.19 Gy for Chiba and from 2.31 ± 0.11 Gy to 3.66 ± 0.17 Gy for Darmstadt. Isoeffective D_{10} doses of gut crypts after single doses ranged from 8.25 ± 0.17 Gy to 10.32 ± 0.14 Gy for Chiba and from 8.27 ± 0.10 Gy to 10.27 ± 0.27 Gy for Darmstadt, whereas isoeffective D_{10} doses after three fractionated doses were 9.89 ± 0.17 Gy through 13.70 ± 0.54 Gy and 10.14 ± 0.20 Gy through 13.30 ± 0.41 Gy for Chiba and Darmstadt, respectively. Overall difference of RBE between the two facilities was 0-5% or 3-7% for gut crypt survival or HSG cell killing, respectively. They concluded that the carbon-ion beams at the NIRS in Chiba, Japan and the GSI are biologically identical after single and daily fractionated irradiation.

1. Beam modulation system
Proton serves advantages with their physical dose distribution which may provide reduced side effects and increased tumor control probability through dose escalation. In clinical practice, the variation of RBE within the SOBP is regarded as negligible in order to have 1.1 as the RBE value. However, as the SOBP is formed by multiple superimposed plateaus and peaks of varying intensity and range, the LETs in the proximal and distal portion of the SOBP must be different. In the proximal area, the proton is of a higher energy and lower LET, while in the distal area the energy lowers to make the LET higher. Meanwhile, the proton beam therapy delivers relatively higher fractional dose for target volumes, and in many cases critical normal structures are close to the volume. As the dose prescribed for a patient is directly related to the selected clinical RBE, an accuracy of 5% is also required for the determination of the RBE [44]. With exceptions, the available experimental data indicate that the RBE of SOBP protons increases with decreasing dose or dose per fraction and the increasing depth in the SOBP, with the magnitude of both effects likely being dependent on the α/β ratios of the target cells or tissues [45]. The variations in SOBP are greater in proton therapy with passive beam modulation system. In the passive modulation system, the particle beam is adapted in 3 dimensions to the target volume only by passive non-variable field shaping elements. The beam shaping devices, such as the brass aperture and range compensator, are the sources of undesired secondary radiation. Meanwhile, the active beam-modulation system, a fine pencil-like beam is used to fill the voxels, which compose the target volume thus the path of the proton beam is not disturbed [46]. This active scanning technique is expected to produce less out-of-field dose when treating the same target volume [20]. In the aspect of RBE in clinical practice, the passive modulation system serves simple way to direct the RBE, because the RBE depth profile remains constant over the treatment field [4]. Thus, the RBE profile can directly be considered in the design of the modulator wheel in the passive modulation system. The active-modulation system is more sophisticated and theoretically, the RBE should be calculated separately for each voxel within the treatment field [47].

2. Proton RBE in Korea
In Korea, only one proton therapy facility is currently opera-
ting at the National Cancer Center. The radiobiological characteristic of the proton beam is reported in 2008 [48]. RBE has been calculated in HSG cells, using clonogenic survival and the MTT assay (cell viability test) at a fixed 190 MeV proton beam with 6 cm SOBP. The reported RBE was 1.024 ± 0.007 by clonogenic assay and 1.049 ± 0.028 by MTT assay. In the report, further analysis of the biological response of proton exposure revealed no difference compared to conventional X-ray treatment on Western blot, and fluorescent activated cell sorter (FACS) analysis. Although the reported RBE of the center was slightly lower than generic RBE 1.1, they still use generic RBE 1.1 as the representative RBE without correction. In 2011, in vivo RBE was reported from the same institution [49]. In the report they changed energy to 210 MeV with same 6-cm SOBP. The RBE was estimated from the survival of jejunal crypt in C3H/He mice. The doses that reduced the number of regenerated crypt per jejunal circumference to 20 (D20) in C3H/He mice were 14.8 Gy for X-rays and 13.5 Gy for protons so that the RBE in the middle of the SOBP was 1.10 in this case.

Outlook

The reason we use RBEs in practice is to bring our inherited clinical experiences of photon beam era into particle beam treatment. However, the RBEs of particle beams, especially for heavy ions, show much dynamic changes according to various factors. The authors hope this contribution may provoke some biological interests for the Korean radiation oncologists’ society on the particle therapies.

Conflict of Interest

No potential conflict of interest relevant to this article was reported.

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