Model Test Research on the End Bearing Behavior of the Large-Diameter Cast-in-Place Concrete Pile for Jointed Rock Mass

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1. Introduction

To improve the end bearing capacity of large-diameter cast-in-place concrete piles, it is best to select rock strata as the bearing stratum at the pile end. Researches by Serrano and Olalla [1, 2], Yang and Yin [3], Saada et al. [4], and Imani et al. [5] focused on the rock mass according to the Hoek-Brown failure criterion, which is applied for intact rocks. However, in practical engineering, the most natural rock masses are made of rock blocks and discontinuous surfaces, and the discontinuity plays an important role in rock deformation and the failure mechanism. However, conducting a destructive test to determine the ultimate bearing capacity of a single pile in a prototype test is cost prohibitive, which limits researchers’ ability to collect sufficient experimental data in order to better understand bearing behavior. This is especially true when the bedrock of the pile end is discontinuous, in which case, even with a large field test, it is very difficult to gather data necessary for a qualitative analysis of the influence of jointed dip angles on bearing capacity. Thus, research needs to focus on how to correctly calculate the end bearing resistance of a single pile in a jointed rock foundation.

At present, some researchers conducted studies on the bearing behavior of jointed rock masses. Reik and Zacás [6] studied the strength and deformation characteristics of jointed media in true triaxial compression. Yang et al. [7] carried out uniaxial compression test of shale rock and found that there are three kinds of failure modes for the jointed rock and that a change in the dip angle caused changes in the failure modes. Yang et al. [8] conducted a uniaxial compression test using marble specimens with prefabricated joints and described the relationship between the dip angle and the failure mode of nonconsecutive jointed rock. Mas Ivars et al. [9] described a new approach they called synthetic rock mass modeling for simulating the mechanical behavior of a jointed rock mass. Zhou et al. [10] fabricated rock-like materials containing multiple fissures under uniaxial compression to further research the effects of preexisting...
fissures on mechanical properties and crack coalescence of rock. Compared with previous experiments, they found five types of cracks, including wing cracks, quasi-coplanar secondary cracks, oblique secondary cracks, out-of-plane tensile cracks, and out-of-plane shear cracks and ten types of crack coalescence. Gao and Kang [11] demonstrated a numerical analysis using a discrete element method simulation for the jointed rock masses. And the numerical results indicate that fracture intensity has no significant influence on the residual strength of jointed rock masses, independent of confining conditions. Cao et al. [12] combined similar material testing and discrete element numerical method (PFC2D) to study the peak strength and failure characteristics of rock-like materials with multifissures. The failure mode can be classified into four categories: mixed failure, shear failure, stepped path failure, and intact failure. And the results show that the peak strength and failure modes in the numerically simulated and experimental results are in good agreement. Yang et al. [13] studied the relationship between the 3D morphological characteristics and the peak shear strength for jointed rock. And a new peak shear strength criterion for rock joints was proposed using two 3D morphological parameters. Furthermore, the calculated peak strengths using the proposed criterion match well with the observed values. Huang et al. [14] did a series of uniaxial compression tests to research the effects of preexisting fissures on the mechanical properties and crack coalescence process for rock-like material with two unparallel fissures. And the strength and deformability characteristics of rock with preexisting fissures are governed by cracking behavior.

Although the above research results could be applied to a jointed rock mass, the results are different from the jointed rock foundation of a pile end that supports the vertical load from the pile and thus produces different failure modes. Kulhawy and Goodman [15] put forward that the spacing of horizontal and vertical joints is the essential factors in the ultimate pile end resistance. Bennmokrane et al. [16] conducted a rock-socketed pile model test and illustrated that when weak interlayered layers exist within the rock mass, the ultimate end bearing capacity is influenced by the different jointed dip angles. Maghous et al. [17] assessed the load bearing capacity of rock foundations resting on a regularly jointed rock and considered the rock matrix and the joints separately. They then compared the obtained results with those derived through considering the jointed rock mass as a homogenized medium. Sutcliffe et al. [18] analyzed the bearing capacity of rock masses containing one to three sets of closely spaced joints. Halakatevakis and Sofianos [19] used a distinct element code to analyze a series of jointed rock samples containing one to three joint sets with various spacing and dip angles and concluded that the strength of the models was independent of the joint spacing. Yu [20] proposed the extended finite element method (XFEM), a numerical method for analyzing discontinuous rock masses that is very convenient for preprocessing. In this model, discontinuities, such as joints, faults, and material interfaces, are contained in the elements, so the mesh can be generated without taking into account the existence of discontinuities. Hossein et al. [21] used distinct element method to build a numerical model to evaluate bearing capacity of strip footing rested on anisotropic discontinuous rock mass. And the results show that the failure mechanism of rock mass depended on both geometrical parameters of joint sets and strength parameters of rock mass.

In order to study the relationship between jointed dip angles and the end bearing characteristics of a single pile, we use discrete element models to simulate the mechanical characteristics of jointed bedrock with different inclination angles. The laboratory model tests are designed to analyze the failure modes, cracking mechanism, and variations in the ultimate end bearing capacity when the jointed dip angles and jointed numbers are changed. The results obtained from the model tests are compared with the numerical analysis results to verify the correctness of the related theory of the failure mechanism of the jointed rock mass.

2. Numerical Analysis of the Failure Mode

2.1. The Theoretical Basis of Discrete Element Method. The failure modes of the jointed rock foundation are simulated with different jointed dip angles according to the discrete element method. Discrete element method (DEM) was firstly proposed by Cundall in 1971. This method is based on the discrete characteristics of material itself to establish numerical model. It shows great superiority in simulating discrete material.

The discrete element program PFC (particle flow code), which can simulate circular particle movement and interaction, is adopted to simulate the failure. The interactional force of particles is calculated according to Newton's second law and the contact law of force. Discrete element analysis considers the following interactional forces: (1) the force of gravity; (2) the contact force between particles and between particles and walls; (3) the frictional force between particles and between particles and walls. The calculated results are compared to the experimental results in order to verify the correctness of the theoretical analysis.

The basic motion equation of the discrete element is built by dynamic relaxation method as

\[
m\ddot{x}(t) + c\dot{x}(t) + kx(t) = f(t),
\]

where \(m\) is the quality of a unit; \(x(t)\) is the displacement of a unit; \(t\) is the time; \(c\) is the viscous damping coefficient; \(k\) is the stiffness coefficient; \(f(t)\) is the external load of a unit. Equation (1) can be changed into the following form as equation (2) by using the central difference method.

\[
\frac{m[x(t+\Delta t) - 2x(t) + x(t-\Delta t)]}{(\Delta t)^2} + \frac{c[x(t+\Delta t) - x(t-\Delta t)]}{2(\Delta t)^2} = f(t),
\]

where \(t\) is the calculating time step and (3) can be obtained by changing (2):

\[
x(t+\Delta t) = \frac{[(\Delta t)^2 f(t) + (c\Delta t/2 - m)x(t-\Delta t) + [2m - k(\Delta t)^2]x(t)]}{(m + c\Delta t/2)}.
\]
The velocity and acceleration of the particles in the time of \( t \) can be obtained by bringing \( x(t + \Delta t) \) into the following two equations:

\[
\dot{x}(t) = \frac{[x(t + \Delta t) - x(t - \Delta t)]}{2(\Delta t)}, \tag{4}
\]

\[
\ddot{x}(t) = \frac{[\dot{x}(t + \Delta t) - 2x(t) + x(t - \Delta t)]}{(\Delta t)^2}.
\]

So it can be seen that the central difference method is used in discrete element method. It is an explicit solution which does not require the solution of a large matrix and saves the computing time. And this method can be used to solve some nonlinear problems.

2.2. Setup Simulation Models and Determination of the Basic Parameters. The model is made up of an end-closed cylindrical container filled with well-compacted round particles and a pipe-shaped model pile. The soil model with a width of \( 10B (W) \) and a height of \( 10B \) is used, where \( B \) is the pile diameter and is equal to 50 mm. And the pile length is 20 mm. The roughness of the pile surface can be set up to simulate the friction coefficient.

The relative parameters of particles are shown in Table 1 obtained by general triaxial test of particle flow code. A set of parameters, which can reflect the macroscopic mechanical behavior of rock mass, are obtained by constantly adjusting the microparameters. And this set of parameters could reflect the strength and deformation characteristics of the rock materials. The rock models, which are composed of balls with the diameters uniformly varying between 2 mm and 3 mm, contained intact rock models and the jointed rock models with the dip angles of 0°, 10°, 30°, 45°, 60°, 75° and 90°, respectively.

| Parameters                  | Rock particles | Joints particles | Pile particles |
|-----------------------------|----------------|------------------|---------------|
| Friction coefficient        | 0.7            | 0.3              | 0.7           |
| Normal contact stiffness (MPa/m) | 1200        | 100              | 2000          |
| Shear contact stiffness (MPa/m) | 400         | 100              | 2000          |
| Parallel-bond normal stiffness (MPa/m) | 4e4        | 2e4              | 1e8           |
| Parallel-bond shear stiffness (MPa/m) | 2e4        | 1e4              | 1e8           |
| Density (kg/m³)             | 2650           | 2650             | 2650          |
| Normal bond stress (MPa)    | 500            | 500              | 1000          |
| Shear bond stress (MPa)     | 500            | 500              | 1000          |

The following assumptions are made to simulate the process of pressing the pile: (1) the particle unit is considered elastomer; (2) the contact points between particles allow a certain amount of “overlap”; (3) compared with the particle size of itself, the “overlap” is very small; (4) the particles of rock mass are spherical unit. The boundary condition of rock mass is built through the “wall” module. The functions of the wall include the following two aspects: (1) to reach the specified initial confining pressure or axial pressure; (2) to maintain a certain confining pressure. The rock model is shown in Figure 1. And the crack distribution, the load transfer path, and the displacement field can be obtained from the results of numerical simulation.

2.3. Crack Distribution. It can be seen from Figure 2(a) that in intact rock the crack distribution is basically symmetrical under upper loading. As loading continues, a compaction
Figure 2: The crack distributions of single-jointed rock mass with different dip angles.
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Table 2: Design parameters of the modeling pile and the rock.

| The numbers | Material ratios (sand : cement : water) | Pile diameters (mm) | Jointed dip angles | Jointed numbers |
|-------------|----------------------------------------|--------------------|-------------------|----------------|
| Group A     | 2 : 1 : 0.6                            | 50                 | 0° 10° 30° 45° 60° 75° 90° | 1              |
| Group B     | 3 : 1 : 0.6                            | 50                 | 0° 10° 30° 45° 60° 75° 90° | 1              |
| Group C     | 2 : 1 : 0.6                            | 50                 | 0° 10° 30° 45° 60° 75° 90° | 3              |

region like a cone will be generated at the pile end, and the cracks next to the compaction region are in a radial distribution. When the jointed dip angles are 0° and 10°, as shown in Figures 2(b) and 2(c), the cracks are distributed mainly above the jointed layer which reduces the end bearing capacity. When the jointed dip angle is 30°, as shown in Figure 2(d), the cracks are still distributed mainly above the jointed layer. When the value of the angle increases, as shown in Figures 2(e), 2(f), and 2(g), the phenomenon becomes more pronounced. It indicates that the cracks in the rock are distributed mainly in the rock where the loading from the pile end is applied directly and the stress of the bedrock is uneven. The rock is thus identified as anisotropic due to the existence of the joints.

2.4. Load Transferring Path. Figure 3 shows that the existence of the joints, which have a filtering effect on the stress in the bedrock, changes the load transfer path inside the bedrock at the pile end. In order to maintain the stability of the bedrock and avoid dislocation of the joints, the stress used to resist the upper load is reduced, which changes depending on the jointed dip angle. When the dip angle is small (0°–30°), the stress delivered from the pile end continues downward at the jointed position, and the stress distribution in the rock mass is the regional average. When the jointed dip angle increases to 45° to 75°, part of the stress is transferred to restrain the mutual movement of the jointed surfaces in order to ensure the stability of the rock mass. The load at the pile end is still mainly borne by the rock mass above the joint, but it is more obvious for the jointed dip angle of 45° to 75°. When the jointed dip angle is 90°, the stress is distributed evenly to the two parts by the joint, the distribution of the stress and displacement is symmetrical, and there is no obvious effect on the bearing capacity.

3. Model Testing

The spacing of joints in rock mass is usually in meters so that the volume unit becomes very large. Because large-scale mechanical testing is difficult to carry out in rock, it is not realistic to directly measure the mechanical properties of the rock. On the other hand, in situ testing of rock masses has greater ability to produce discreteness in results, so laboratory testing with similar materials could be conducted systematically in order to control the parameters and obtain reasonable mechanical properties. Thus, laboratory testing is widely used for studying the strength, deformation, and failure mechanism of jointed rock masses. In order to analyze the stress, deformation, and failure mechanism of the jointed bedrock more intuitively, a laboratory test was created for a cast-in-place concrete pile to obtain the data regarding different jointed distributions, the ultimate bearing capacity, and the Q-S curves of a single pile.

3.1. The Determination of Experimental Materials. In this test, the pile body is simulated using a solid steel bar with the elastic modulus E of 210 GPa, which ensures that the pile will not be destroyed before the destruction of the bedrock. Considering the feasibility of the model test and the limitation of the site, the test uses as the model materials sand, cement, and water mixed to a specific ratio to form a mortar. Mixed ratios of similar materials are obtained by making standard test blocks and measuring the stress-strain curves to ensure that stress-strain curves similar to natural rock could be adopted. In order to determine the most suitable mixed ratios, different ratios were created. At the end, two ratios were selected as most suitable for the test because of their similarity to natural rock (sand : cement : water = 2 : 1 : 0.6 and 3 : 1 : 0.6). The uniaxial compressive strength of the prepared materials after 28 days is 6 MPa, the unconfined compressive strength (σc) of the simulated rock material is 6 MPa, and the elastic modulus Er is 680 MPa.

3.2. The Experimental Design

3.2.1. The Loading Devices. Taking into consideration the influence of pressing the pile into the bedrock, the size of the experimental model was determined to be 500 mm × 500 mm × 500 mm (length × width × height). So the loading box size was 520 mm × 520 mm × 520 mm (length × width × height). Four steel plates' size of 490 mm × 490 mm was used around the testing block to constrain the horizontal displacement. The thickness of the steel plates was 20 mm, and they were fixed by the mutual pulling of long high-strength screws and solid steel squares to provide lateral confinement. The size of the bottom steel plate was 600 mm × 600 mm with a thickness of 20 mm. In order to reduce the friction between the loading box and the testing block, a lubricant was used between the plates and the rock. The loading system is shown in Figure 4 with a maximum measuring range of 200 t as the loading device, and the loading box is shown in Figure 5. The designing parameters of the modeling pile and the rock are shown as in Table 2.

3.2.2. The Making of the Jointed Testing Blocks. The jointed testing blocks were created using a cutting method. The positions of the joints were marked on the testing surfaces before cutting. After cutting the joints of the blocks, rubber membranes and rubber bands were used to hold up them in order to ensure the overall stability. Then the rock model
Figure 3: The displacement distributions of single-jointed rock mass with different dip angles.
4.2. The Wedge Failing Forming. The load-carrying mechanism of the pile can be regarded as a local compression problem when the load is on the top of the pile and the weight of the overlying soil layer is relatively small. The failing process of the intact bedrock is shown in Figure 8. Firstly, the upper load is transferred to the end of the pile, and the rock mass under the pile is continuously pressed until it is crushed. Under sustained loading, the interface of the pile and the rock generates shear force. When the shear stress exceeds the shear strength, the rock will fail along a rupture angle ($\theta$). At this point, a wedge failing form appears in the rock at the pile end, and the wedge splitting failure of the bedrock is produced under the local pressure load. However, the shape of the wedge differs according to the different dip angles. As shown in Figure 9, the jointed dip angles are, respectively, 0° and 75°. It is obvious that the height of the wedge becomes smaller

(continued in the next section)
as the jointed inclination angle increases and the shape of the wedge is asymmetrical, which is caused by the uneven distribution of the shear stress at the end of the pile.

4.3. Force-Displacement Curves (Q-S Curves). In general, the ultimate end bearing capacity is determined when the displacement of the pile top corresponds to the pile diameter by 10%. However, the pile diameters in this model test are extremely small, and the calculated value is less than 9 mm. Given that the model pile is different from the pile in practical engineering, the final loading value of the pile top is used to represent the bearing capacity of a single pile. In the early stage of loading, the joints of the rock experienced the process of closure regardless of the size of the dip angle.
Thus the curves of the load and displacement have shown a nearly linear relationship and gradually change to a nonlinear relationship as the rock becomes deformed, and there are obvious turning points in the Q-S curves as shown in Figures 10 and 11.

The deformation of the jointed rock mass can be divided roughly into the following four phases: (1) structural adjustment and jointed closure: the original cracks and the joints are closed, and the rock is compressed to format the early nonlinear deformation. (2) Elastic deformation and crack stable development: the curve of this phase is similar to the linear phase, and, according to the deformation mechanism, it can be subdivided into the elastic phase and the stable developing phase of micro cracking. (3) Unstable development: the strength of the joint reaches the ultimate strength, and relative sliding occurs at the jointed surfaces and microcracks continue to develop. Due to the effect of the stress concentration caused by the cracking process, cracking will continue to develop even if the external load remains constant. (4) Destruction: when the bedrock reaches the ultimate bearing capacity, its internal structure is destroyed. In this phase, cracks develop rapidly and form macroscopic cracks. At this point, rock deformation manifests mainly in the relative sliding of rock blocks along the surface of the macro cracks, and the bearing capacity decreases as deformation increases. Even so, the load value is never reduced to zero, since it is clear that the jointed rock mass still has some bearing capacity. As seen from the entire curve, for example, of Figure 10(f), the rock mass reaches the ultimate load relatively slowly, but the failing rock mass retains some residual stress because of the structural effect.

The test can also help obtain the relationship between the different jointed dip angles and the end bearing capacity of the rock. As the jointed dip angles increase from 0° to 90°, the settlement for the pile end first increases and then decreases under the same load. For example, when the load is 200 KN the settlements of the pile end for the jointed bedrock models of group A, as shown on Figure 10, are 3.6 mm, 3.8 mm, 3.9 mm, 4.3 mm, 6.5 mm, 6.3 mm, and 6.1 mm and 4.0 mm. The results indicated that the existence of the joints made the settlement of the pile end. And the phenomenon is more obvious when the jointed dip angles are 45°, 60°, and 75° as seen in Figures 10(e), 10(f), and 10(g). In fact, the increments of jointed bedrock include two parts: the compression of rock and the slip of joint surface. When the jointed dip angles are 45°, 60°, and 75°, the increments caused by the slip of jointed surface are increased. And the Q-S curves of Figure 11 show the same phenomenon as in Figure 10. But when the jointed dip angles are 90° the existence of the joints has no obvious influence on the settlement of pile end.

From Figures 10 and 11, it can be found that the settlements of three-single-joint rock are larger than that of a joint rock when the load is same. The deformation characteristics of the jointed rock mass can be obtained by comparing the Q-S curves such as a single joint of 45° (Figure 10(e)) and three joints of 45° (Figure 11(e)). The shapes of the Q-S curves before reaching the peak strength are approximately the same for the single jointed bedrock and the single set of multiple joints bedrock, but the slope for the single-jointed rock is larger than that for the three-jointed rock, which shows that the deformation capacity of the single-jointed rock mass is better than that of the single set of jointed rock mass. This
Figure 10: Continued.
also indicates that the ultimate bearing capacity of the single-jointed rock mass is much better than that of the three-jointed rock mass.

In addition, the Q-S curves for intact bedrock are shown as in Figure 12(a) and the Q-S curves for jointed bedrock with the dip angle of 45° are shown as in Figure 12(b). The Q-S curves show that the simulating results are in good agreement with the testing results. It also shows that the discrete element method can simulate the end bearing behavior of the jointed bedrock.

4.4. Load-Bearing Characteristic

4.4.1. The Effect of the Rock Strength on the Ultimate End Bearing Capacity. In order to determine the relationship between the ultimate end bearing capacity of the pile and the rock strength the data obtained in the test were plotted, as shown in Figure 13, where the whole curve shows a “V” shape. And the order for end bearing capacity of the jointed rock mass of group A from being high to low is those with the dip angles of 90°, 0°, 30°, 45°, 60°, and 75°, respectively; the order for end bearing capacity of the jointed rock mass of group B from being high to low is those with dip angles of 0°, 90°, 30°, 45°, 60°, and 75°, respectively. The comparison of the bearing behavior of the pile end with the intact bedrock shows that the existence of joints reduces the end ultimate bearing capacity regardless of the arrangement of the joint dip angles. The ultimate end bearing capacity of the intact rock is 415 KN from the test result. And the ultimate end bearing capacity of jointed rock at a 45° angle is 268 KN, which is a reduction of 35.4%. These results also indicate that the existence of joints in the rock foundation leads to significant anisotropy. Moreover, the strength of the rock decreases in the presence of joints even if the jointed surface is perpendicular to the direction of maximum principal stress. However, the effect of horizontal joints on the strength of the rock is not accidental; rather, it can be attributed to the friction and the binding effect of the jointed surface.

Comparing the different strengths of the bedrock in group A and group B, the rock strength clearly has an influence on the end bearing capacity, namely, that the ultimate end bearing capacity increases as the rock strength increases when the jointed dip angle is determined. It can be seen from Figure 13 that no matter how much the jointed dip angle is the end bearing capacity of group A is greater than that of group B. The reason is that the increasing of rock strength could increase the ability of the bedrock to resist upper load to a certain extent. But when the jointed angles of the bedrock are 45°, 60°, and 75°, the end bearing capacity does not improve significantly with the increasing of rock strength, which indicates that the jointed dip angles of bedrock are the main influence factor to the end bearing capacity.

4.4.2. The Effect of the Jointed Number on the Ultimate End Bearing Capacity. Figure 14 shows that the ultimate bearing capacity of the pile end differs when the rock has the same jointed dip angles, but different jointed numbers. And the order for bearing capacity of the jointed rock mass of group C from being high to low is those with dip angles of 0°, 90°, 30°, 45°, 60°, and 75°, respectively. The curves show that the same trend exists between single-jointed rock and multiple-jointed rock, which still exhibits a “V” shape. But the end bearing capacity decreases as the jointed numbers increase. The reduction in strength is obvious when the number of joints increases from 1 to 3, that is, from the rock with a single joint to the rock with multiple joints. The reason is that the increasing of the joints number of leads to the destruction of integrity of the bedrock. Furthermore, the anisotropy becomes more significant.
Figure 11: Continued.
5. Conclusion

Based on the above analysis about the intact rock foundation and the jointed rock foundation, the following conclusions can be drawn:

(1) The failure mode of the bedrock changes with the existence of the joints. The test results show that the jointed dip angles can change the crack distribution during the process of load transfer. When the jointed dip angle is small, less than 30°, the joints have no significant effect on the destruction of the bedrock; when the jointed dip angle becomes large, greater than 30° and less than 75°, the cause of cracking includes rock compression and sliding of the jointed surfaces; and when the cracks are parallel to the direction of the dip angle, at 90°, the expansion of the cracks is mainly the result of rock compression.

(2) The load transfer path of the bedrock changes because of the joints. When the jointed dip angle is small, the change of the path is not obvious, but when the angle is between 45° and 75°, the change is obvious.

(3) The wedge failing mode of the bedrock generally occurs at the pile end, and the shape of the wedge also changes according to changes in the jointed dip angles.

(4) The overall shape of Q-S curves for jointed rock is approximately the same. However the direction of the curve changes with variations in the jointed dip angles.
and the turning point of the Q-S curves can change in response to changes in the jointed numbers and strength. The jointed angles affect the ultimate bearing capacity of the pile end, which increases as rock strength increases. However, when the jointed dip angle of the bedrock is $45^\circ$ and $60^\circ$, the end bearing capacity does not improve significantly, indicating that the jointed dip angles of the rock foundation are controlled mainly by the load-bearing capacity.

**Competing Interests**

The authors declare that they have no competing interests.

**Authors’ Contributions**

For the research work, Jingwei Cai and Xinsheng Yin conceived and designed the experiments; Jingwei Cai, Xiaxin Tao, and Shibo Tao performed the experiments and analyzed the data; Xinsheng Yin and Aiping Tang contributed the test materials and analysis tools; Jingwei Cai wrote the paper.

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