Weakly Interacting Massive Particles (WIMPs, $\chi$) are candidates for Dark Matter. WIMP searches at lepton colliders are complementary to searches at hadron colliders and direct detection, since they directly probe the coupling to electrons which a priori is independent of the coupling to hadrons. Like at hadron colliders, WIMP pair production can be observed via an additional visible particle, in particular a photon from initial state radiation ($e^+e^- \rightarrow \chi\chi\gamma$). With this technique WIMP masses to nearly half the centre-of-mass energy can be probed. Polarised beams are essential to reduce Standard Model backgrounds and to characterise the properties of the new particles in case a signal is discovered. Prospects for a mono-photon WIMP study at the International Linear Collider will be discussed in the context of EFT. In addition, detector requirements critical to this analysis are discussed.
1. Introduction

The International Linear Collider (ILC) is a future electron-positron collider with a mature technology [1]. Currently, a political decision in Japan is awaited. The centre-of-mass energy can be tuned between 250 GeV and 500 GeV and is upgradable to 1 TeV. The instantaneous luminosity for $\sqrt{s} = 500$ GeV is $1.8 \times 10^{34}$ cm$^{-2}$s$^{-1}$ which can be doubled to $3.6 \times 10^{34}$ cm$^{-2}$s$^{-1}$ after a luminosity upgrade. Both the electron and positron beams are foreseen to be polarised to at least $\pm 80\%$ and $\pm 30\%$, respectively. The ILC will have one interaction region which will accommodate the two foreseen detectors in a push-pull scheme. The presented study is performed for the International Large Detector (ILD) [2].

At colliders, WIMPs could be pair produced. Since the WIMPs do not leave signals in the detector an additional particle is required to detect the process, for example a photon from initial state radiation (ISR). We look for the signal process $e^+e^- \rightarrow \chi\chi\gamma$ whose signature is a single photon in an otherwise "empty" detector. This approach is quasi model-independent. Due to the known initial state, the missing four-momentum can be calculated using two observables, namely the photon energy $E_\gamma$ and the photon polar angle $\theta_\gamma$.

![Figure 1: Pseudo-Feynman diagram for the signal process and example Feynman diagrams for the two main background processes: radiative neutrino pair production and Bhabha scattering.](image)

The two main background processes are neutrino pair production and Bhabha scattering, both with an associated photon from initial state radiation, or in the latter case also from final state radiation (see fig.1). The neutrino background is irreducible, but can be enhanced or suppressed by changing the polarisation combination. Bhabha scattering has a huge cross section and mimics the signal if both leptons escape undetected. For the suppression of this background process the best possible hermeticity in the forward region of the detector is required.

2. Motivation for an ILC Simulation Study

The theoretical framework used in this analysis are effective operators, where the underlying idea is to classify the WIMP based on its quantum numbers (spin and weak isospin) and the mediator by its spin and construct the minimal effective Lagrangian. The only parameter that remains, $\Lambda$, can be called the energy scale of new physics and is a function of the mediator mass and the coupling to the fermions $g_f$ and the coupling to the WIMPs $g\chi$: $\Lambda = M_{\text{mediator}}/\sqrt{g_f g_{\chi}}$.

In such a framework, considering the full Lagrangian, a likelihood analysis of data of existing experiments, together with extrapolations of expected exclusion limits at the time the ILC is running is being performed. Figure 2 shows the surviving region assuming that no WIMP signal is detected, for the example of a singlet-like fermion WIMP [3]. Data from the following experiments are considered: from the Planck satellite, from the direct detection experiments PICO-2L,
LUX and XENON100, from collider searches at LEP and LHC and from future experiments like LZ and PICO250. Here, the couplings are tested in the range [-1,1]. Above the grey area this simplified model reproduces the results of effective operators. The yellow region shows the parameter space which will not be explored by other experiments before the ILC starts.

![Figure 2](image.png)

**Figure 2**: The parameter space which will not be covered by dark matter experiments by the time the ILC will be running is shown in yellow (68% confidence level) and blue (95% C.L.). The computations are based on extrapolations of current and future experiments assuming that no WIMP signal is detected. The grey area reflects the parameter space in which the approach of effective operators is not valid: $\Lambda$ has to be larger than three times the WIMP mass and above 300 GeV. [3]

3. Modelling of Signal and Background

The signal definition in this analysis comprises three requirements on the photon: a minimum energy of 10 GeV, a maximum energy of 220 GeV and $|\cos \theta_\gamma| < 0.98$. The upper cut on the energy is applied to avoid the large background rates in the region close to the radiative return to the Z boson, which corresponds to $E_\gamma = 242$ GeV for $\sqrt{s} = 500$ GeV. The angle is restricted to the parts of the detector in which the tracking performance guarantees that photons can be distinguished from electrons and positrons.

The events are generated using WHIZARD version 2.2.8 [4], with the matrix element generator O’Mega [5]. Polarised beams are included as well as the beam energy spectrum. The generated background processes are neutrino pairs plus several photons and for the Bhabha scattering electron-positron pairs plus several photons. The signal events $\chi\chi\gamma$ are obtained by reweighting the $\nu\bar{\nu}\gamma$ events using the differential cross section formulas expressed in terms of the WIMP mass and spin.

For modelling the photons, WHIZARD offers an ISR parametrisation that comprises all orders of soft-collinear photons and the first three orders of hard-collinear photons. With this the cross sections of the considered processes are calculated with high accuracy. However, a realistic distribution of the photon polar angle is obtained by including the photons in the matrix element. By doing so, double counting of photons is avoided. Both approaches are combined by generating the events with the photons in the matrix element and reweighting the cross section to the one with the ISR parametrisation.

The events are simulated in a Geant4 based simulation of the full ILD detector model presented in the Technical Design Report [2].
4. Results

4.1 Higher Sensitivity with Improved Bhabha Rejection

Signal-like events with only very little detector activity besides the photon are selected by requiring the following three criteria. There must be no tracks with a transverse momentum exceeding 3 GeV. The visible energy, excluding that of the photon, has to be smaller than 20 GeV. Finally, there must be no electrons and positrons detected in the forward region, or more technically speaking: no clusters may be reconstructed in the forward detector BeamCal.

Table 1 shows the percentage of Bhabha scattering events surviving the three conditions, for the full analysis done in 2013 [6] (central column) together with our update of the analysis. In the new analysis the Bhabha background is suppressed to a sub-permille level with respect to the signal definition, which is approximately fifteen times more effective compared to the last analysis. The requirement of a low visible energy leads to an eight times higher rejection, which is due to improvements in particle flow and photon reconstruction. With an optimised BeamCal reconstruction algorithm [7], an additional factor of two is achieved. This shows that both detector resolution and detailed reconstruction are crucial for a reliable performance estimate.

Figure 3 shows a comparison between the previous sensitivity [8] which is based on the background rejection efficiency of [6] (red dashed line) and our update (blue solid line). For right-handed electrons and left-handed positrons the level of the exclusion limit can be improved by up to 300 GeV in $\Lambda$, for a centre-of-mass energy of 500 GeV and an integrated luminosity of 500 fb$^{-1}$.

### Table 1: Fractions of signal-like Bhabha scattering events surviving the three conditions for an "empty" detector. The central column shows the latest full analysis [6] and the right one our update.

| $e^+e^-\gamma$ | [6] | new analysis |
|-----------------|-----|--------------|
| $p_T$           | 21.1 % | 26.1 %       |
| $E_{\text{vis}}$ | 16.0 % | 1.9 %        |
| BeamCal         | 0.29 % | 0.02 %       |

4.2 Impact of the Forward Detector Design

High numbers of electron-positron pairs created from beamstrahlung hit the inner part of BeamCal. As a consequence, the reconstruction efficiency of particles coming from the hard interaction decreases dramatically at very low polar angles $\theta$. The identification of Bhabha scattering events hence strongly depends on the design of the forward region.
Because the ILC detectors share the same interaction region, both are required to have the same focal distance of the final quadrupole magnet (L*). In order to equalise that length for both detectors, the forward region of the ILD detector is currently being redesigned [9]. BeamCal has to be moved closer to the interaction point by 40 cm. While the detailed redesign and the implementation in the ILD simulation is ongoing, we estimate the impact in the following way: Firstly, we assume that area in BCal polluted by the pairs is the same for all considered distances. Secondly, the lepton reconstruction efficiency is approximated to be 100% for polar angles above an effective angle \( \theta_{\text{eff}} \) and 0% below. The number of events with both leptons not being reconstructed using the full detector simulation corresponds to an effective angle of approximately 15.5 mrad. With these assumptions, the hermeticity in the forward region depends purely geometrically on the distance of BeamCal to the interaction point. This means that the effective polar angle grows linearly with the distance by which BeamCal is moved in towards the interaction point.

Figure 4 shows how the number of Bhabha scattering events with both leptons not being reconstructed changes as a function of the effective polar angle. With the new position of the subdetector, the Bhabha background would be three to four times higher. With this higher background level the improvement presented in section 4.1 would be partially lost.

4.3 Sensitivity in Different Operation Scenarios

Based on the results of the previous study [6] performed at \( \sqrt{s} = 500 \text{ GeV} \) and 500 fb\(^{-1} \) we developed a scheme to extrapolate the results to other energies and integrated luminosities. This extrapolation is restricted to WIMP masses below 100 GeV, where the sensitivity does not depend on the WIMP mass. This study allows to give estimates of the sensitivity for different time scales and different running scenarios, i.e. how much integrated luminosity is collected at which centre-of-mass energy, in which order this occurs and how the integrated luminosity is distributed between the different polarisation combinations (fig. 5).

The running scenario H-20 [10] starts with \( \sqrt{s} = 500 \text{ GeV} \) at which initially 500 fb\(^{-1} \) are collected (fig.6). After the first four years an exclusion limit of \( \Lambda \approx 2.5 \text{ TeV} \) is reached for a vector-like fermion WIMP and a vector-like operator. When ignoring the contributions of the other centre-of-mass energies, this exclusion limit grows during a second run at \( \sqrt{s} = 500 \text{ GeV} \) after a luminosity upgrade. After the full ILC programme the runs at \( \sqrt{s} = 500 \text{ GeV} \) will have contributed to an exclusion limit of \( \Lambda \approx 3 \text{ TeV} \). With an upgrade to \( \sqrt{s} = 1 \text{ TeV} \) the reachable \( \Lambda \) is approximately 4.5 TeV.
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Figure 5: Extrapolation of the exclusion limits from the full simulation to the full range of ILC centre-of-mass energies and different integrated luminosities, for fractions of 22.5% (left) and 40% of the data collected with right-handed electrons and left-handed positrons.

The sensitivity strongly depends on the fraction of the integrated luminosity collected with right-handed electrons and left-handed positrons for which the neutrino background is strongly suppressed. The rather large fraction in H20 (40%) is clearly favoured over 22.5% (compare fig. 5).

A full update of the whole analysis to the new detector performance for all types of WIMPs is underway.

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