Natural Disasters and Macroeconomic Performance

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Abstract Recent empirical research has shown that output and GDP per capita in the aftermath of natural disasters are not necessarily lower than before the event. In many cases, both are not significantly affected and, surprisingly, sometimes they are found to respond positively to natural disasters. Here, we propose a novel economic theory that explains these observations. Specifically, we show that GDP is driven above its pre-shock level when natural disasters destroy predominantly durable consumption goods (cars, furniture, etc.). Disasters destroying mainly productive capital, in contrast, are predicted to reduce GDP. Insignificant responses of GDP can be expected when disasters destroy both, durable goods and productive capital. We extend the model by a residential housing sector and show that disasters may also have an insignificant impact on GDP when they destroy residential houses and durable goods. We show that disasters, irrespective of whether their impact on GDP is positive, negative, or insignificant, entail considerable losses of aggregate welfare.

Keywords Natural disasters · Economic recovery · Durable goods · Residential housing · Economic growth

JEL Classification E20 · O40 · Q54 · R31

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1 Introduction

In this paper, we propose an economic theory to analyze the macroeconomic effects of natural disasters. We mainly focus on hydro-meteorological disasters (e.g. floods, storms, droughts) and geophysical disasters (e.g. earthquakes, tsunamis), and the physical and monetary damage caused by these disasters. As documented by Cavallo and Noy (2011), these types of disasters are fairly common events across the globe, and occur with increasing frequency. For example, in the Asia-Pacific region, the most afflicted region, the incidence of natural disasters increased from 11 events per country in the 1970s to 28 events in the 2000s. In Western Europe, events per country and decade increased from 5 to 15 over the same time period.

To date, there exists a large and increasing empirical literature investigating the economic impact of natural disasters (e.g. Raddatz 2007; Noy 2009; Loayza et al. 2012; Fomby et al. 2013; Cavallo et al. 2013; Felbermayr and Göschl 2014; Cavallo and Noy 2011 for a survey). One perhaps surprising conclusion suggested by the literature is that disasters do not necessarily decrease output and GDP per capita in the subsequent three to five years after the event. Loayza et al. (2012), for example, find no significant impact on a country’s GDP and industrial output across all disasters. In contrast, when floods are investigated separately, they are found to stimulate GDP while droughts are found to harm GDP in developing countries (but not everywhere). Similarly, Fomby et al. (2013) find a positive effect of floods and a negative effect of droughts but no effect of earthquakes and storms on post-disaster GDP in developing countries. Using counterfactual analysis, Cavallo et al. (2013) find that disasters exert no significant influence on medium-run and long-run output when they control for potential post-disaster outbreak of social conflict.

These empirical observations seem puzzling when analyzed within the context of conventional neoclassical growth theory. Once we acknowledge that disasters destroy (potentially severely) the productive potential of an economy, we would expect that they harm subsequent economic performance. It is true that the neoclassical growth model predicts that the growth rate after an exogenous loss of capital stock (or other productive factors) is positive. This phenomenon is known as catch-up growth from below towards the steady state. GDP per capita, however, is predicted to fall short of its pre-disaster level according to conventional growth theory.1

In this paper, we show how a simple extension of the neoclassical growth model can be used to reconcile theory with empirical evidence and how the model can be used to motivate the diverse post-shock macroeconomic outcomes found in the disaster literature. The key ingredients are the introduction of variable labor supply and the distinction between productive capital stock and durable goods (like cars, furniture, or household appliances). In line with conventional theory, the model predicts that an exogenous loss of capital stock reduces post-disaster GDP. An exogenous loss of durable goods, in contrast, drives GDP above its pre-shock level. The reason is that individuals, suffering from the implied negative wealth shock, supply more labor. On the other hand, households want to (quickly) rebuild the stock of durable goods. The higher level of durable goods investment during the reconstruction phase also lifts labor demand. Higher employment in conjunction with an undestroyed capital stock implies higher output per capita during the reconstruction phase.

1 The disaster literature, confusingly for growth economists, refers sometimes to the differential between pre- and post-shock levels of GDP as GDP growth (e.g. Loayza et al. 2012). This differential is predicted by the standard neoclassical growth model to be unambiguously negative. Moreover there exists also a smaller literature investigating the association between disaster risk and long-run growth (e.g. Skidmore and Toya 2002; and Crespo Cuaresma et al. 2008). Here, we focus on the medium-run impact of disasters.
Considering simultaneous shocks on both state variables, the model predicts a negative impact on GDP for disasters destroying predominantly productive capital and a positive impact on GDP for disasters destroying predominantly durable goods. No significant effect on GDP is predicted when the effects on firm capital is somewhat smaller compared to that on durable goods. The theory is not only helpful to explain the frequently insignificant impact of disasters on GDP, it can also rationalize those cases for which the literature finds significant GDP effects. Intuitively, we may expect that droughts exert a negative impact on GDP because they leave durable goods mostly intact and destroy predominantly firm capital. This is in particularly the case in largely agrarian societies (where capital stock consists of seeds, livestock etc.). Conversely, we expect that floods are more likely to stimulate GDP because they damage predominantly durable goods like cars, furniture or household appliances. In support of our proposed mechanism, some studies have documented positive employment effects of disasters (Leiter et al. 2009; Ewing et al. 2009).

In order to present the mechanics behind the “durable goods–channel” in the cleanest way we first discuss the case of a small open economy with perfect capital mobility. This shuts down the “capital-channel” because the capital stock is pinned down to its steady-state value. In this framework, we generally prove that disasters damaging durable goods lead to higher GDP in the short and long run. We then turn to the case of a closed economy and show that the main mechanics are preserved while another amplifying effect occurs through intertemporal substitution. Households want to reconstruct their destroyed stock of durable goods quickly and increase their durable goods purchases in the aftermath of the disaster. Since international capital markets are no longer available to smooth consumption, resources for this purpose are freed by reducing investments in productive capital and by reducing consumption of nondurable goods. In order to mitigate the drop in consumption, households are motivated to raise their labor supply even further than in the case of a small open economy.

Because disasters may not only destroy physical capital and durable goods but also houses, we extend the benchmark model by residential housing. We show that the main mechanisms generating a negative, insignificant, or positive impact of disasters on output are still at work in the extended model. Furthermore, the model offers an additional channel through which a disaster might leave GDP unaffected: if a disaster leaves physical capital intact but destroys durable goods and residential housing, there exists a positive impact on GDP through higher labor supply, and a negative impact on GDP through a lower service flow from housing. When both effects balance each other, GDP is predicted to remain unaffected by a disaster.

Our analysis of the individual effects of disasters on firm capital, durable goods, and residential housing shows that GDP can be a very misleading indicator of the economic damage caused by natural disasters. This is most obvious when we compare a disaster that destroys “only” productive capital with another one destroying additionally durable goods (and residential housing). The GDP damage is larger for the first one while the welfare loss is larger for the second one. In order to discuss these outcomes explicitly, we augment the quantitative discussion of our disaster economies by a welfare analysis and show large welfare losses from disasters that leave GDP more or less unaffected.

There exists a small theoretical literature assessing the general economic impact of disasters (West and Lenze 1994; Rose and Liao 2005; Henriet et al. 2012). These studies focus mainly on a sectoral decomposition of the impact of disasters and do not try to explain the (potentially non-negative) impact of disasters on aggregate GDP. Crespo Cuaresma et al. (2008) speculate that disasters may exert a positive impact on GDP through creative destruction. The proposed mechanism works through opportunities to update the partially destroyed capital stock. However, scrutinizing the mechanism in a theoretical model, Hallegatte and Dumas (2009) found that it cannot account for a positive response of GDP on disasters.
Another strand of related literature discusses how mitigation policies affect the economic consequences of disasters (see e.g. Kellenberg and Mobarak 2008; Hallegatte 2013, and Posch and Trimborn 2013). Ex ante mitigation in response to disaster risk exposure is certainly an important aspect for a proper quantitative assessment of the impact of disasters on GDP. In the context of our model, however, it is important to emphasize that taking ex ante mitigation into account would not change any of our qualitative results. Mitigation would reduce the amount of capital and durable goods that get destroyed by a disaster but it would have no effect on the relation between the type of destroyed assets and GDP growth in the aftermath of the disaster, which is the focus of our study.

The paper is organized as follows. In Sect. 2 we present supporting evidence on the association between the type of disaster and its impact on GDP. In Sect. 3 we introduce the general model, in Sect. 4 we discuss the case of a small open economy, and in Sect. 5 we discuss the closed economy case. In Sect. 6, we specify the model numerically and investigate post-disaster adjustment dynamics quantitatively. We provide estimates of the disasters’ impact on GDP and aggregate welfare under varying assumptions about the physical impact of disasters. Throughout the paper we focus on economic or “material” effects and ignore the fact that natural disasters kill people. The welfare estimates should thus be understood as lower bounds of the actual damage caused by natural disasters. In Sect. 7 we extend the model by a residential housing sector. In the main text, we assume that households own their houses. In the “Appendix”, we show robustness of results against an alternative setup in which households rent housing services from firms. Section 8 concludes.

2 Disaster Damage and GDP

In this section we draw on empirical evidence to corroborate the main mechanism of our model. Ideally, we would like use information on the damage of disasters classified by impact on durable goods and productive capital stock. Since these data are unfortunately unavailable we have to rely on (narrative) discussion of examples and suggestive evidence on the association between durable goods expenditure and GDP growth in the aftermath of disasters.

We start by distinguishing two post-disaster phases. The short run is characterized by the immediate aftermath of the disaster which can last from a few days up to several months. The medium run is characterized by the post-disaster catch-up phase, which may last up to several years. In the immediate aftermath of the disaster, people in affected areas try to organize shelter, guard remaining possessions, fix whatever can be fixed in home production, and try to organize emergency goods (e.g. food, candles, sleeping bags etc.). Thus people may temporarily retreat from the formal labor market and focus on home production. In combination with disruptions in the production process the immediate response of GDP to a disaster is expected to be negative. Felbermayr and Göschl (2014) confirm this conjecture by showing that the impact of disasters on GDP is negative in the first year after the disaster. Here, we focus on the medium run, as the majority of the empirical literature on the impact of disasters on GDP (cited in the Introduction). Most of these studies consider a time horizon of three to five years after the strike of disasters. In the medium run, the immediate impact phase, while still included, is dominated by the modification of plans of forward-looking individuals and their consequences for aggregate adjustment dynamics towards the new steady state of the economy. As motivated in the Introduction, we argue that the response of GDP in the medium run crucially depends on which type of asset got destroyed by the
disaster. Since this information is not available, we focus on specific disasters for which we can infer which type of asset was mainly destroyed.

We start by discussing, as an example, a disaster that mainly destroyed physical capital and infrastructure. For this type of disaster we would expect the adjustment process familiar from standard growth economics according to which GDP declines in the aftermath of the disaster and converges towards the pre-disaster steady state level from below. We choose the Great East Japan earthquake, a combination of a severe earthquake and a Tsunami that hit Japan on 11. of March, 2011. The disaster destroyed a large number of production sites, roads, bridges, railways, and power plants. The total damage has been estimated as a loss of about 5.7% in terms of GDP and 2% in terms of aggregate capital stock. The destruction of capital and infrastructure caused a shortfall of production and a disruption of the supply chains in the manufacturing sector. In addition, factories and households were plagued by electricity shortfalls caused by the blackout of the Fukushima nuclear plant (Nanto et al. 2011; Norio et al. 2011).

Evaluating the impact of the disaster on GDP only by comparing GDP averages of the years before and after the disaster could be misleading because the disaster hit Japan on the recovery path from the Great Recession, implying that trend growth might have been higher than usual. Fortunately, pre-disaster GDP forecasts up to the second quarter (Q2) of the year 2012 are available such that we can compare forecasted with actual GDP. The disaster caused Japan’s GDP to drop for about 2% in Q1 and Q2 2011 compared to the pre-disaster forecasts (see Wieland2016, Figure 4a). It remained below the pre-disaster estimates at least until Q2 2012, the latest date for which pre-disaster forecasts are available. This indicates that the Great East Japan earthquake had a negative impact on GDP.

Another way to carve out the impact of this disaster on the Japanese economy is to focus on components of GDP which are mostly affected by physical capital losses. Since manufacturing is more capital intensive compared to services, we target Japan’s index of industrial production excluding construction. The index recovered after the Great Recession and reached a high in Q3 and Q4 2010. It declined when the disaster hit (Q1, 2011), reached a low in Q2, 2011 of more than −10 percentage points, and never recovered to the level of Q3/Q4 2010 again. This indicates that the destruction of capital caused by the earthquake and tsunami had a long-lasting negative impact on industrial output.

We next present evidence supporting our suggested mechanism through which disasters that destroy mainly durable goods exert a positive effect on GDP. We focus on floods because Loayza et al. (2012) and Fomby et al. (2013) document that floods are most likely to exert a positive effect on output and GDP. Constraint by data availability, we focus on floods that hit the U.S. between the years 2000 and 2010 (see Dartmouth Flood Observatory). We restrict the sample on those disasters meeting the following two criteria: First, the main damage resulted from flooding, and not from collateral disasters like storms. Second, either the total damage from the disaster exceeds 200 million US$ or the average per capita damage of the most affected state exceeds 15,000 US$. The flooding events are the Allison flood (2001), the LA country flood (2005), Hurricane Katrina (2005), the Mid-Atlantic and New England flood (2005), the Mid-Atlantic flood (2006), the Midwest flooding (2007), the Oregon and Washington flood (2007), the June Midwest flood (2008), the Alaska flood (2008), and the Southern flood (2009).

There is no data available on the destruction of durable goods. We thus try to infer it from the change in household expenditure on durable goods in the aftermath of the disasters. Figure 1 shows the association between the change in spending on furniture and durable household equipment and the change of GDP per capita in the U.S. state most affected by the disaster. Data for GDP and durable goods expenditure at the state level are taken from
Fig. 1 Association between growth of GDP per capita and growth of per capita spending on furniture and durable household equipment. Both values are expressed as percentage change from the average of five years before the disaster and five years after the disaster for the affected US state in relation to the US average. The flooding events are (1) the Allison flood (2001), (2) the LA country flood (2005), (3) Hurricane Katrina (2005), (4) the Mid-Atlantic and New England flood (2005), (5) the Mid-Atlantik flood (2006), (6) the Midwest flooding (2007), (7) the Oregon and Washington flood (2007), (8) the June Midwest flood (2008), (9) the Alaska flood (2008), and (10) the Southern flood (2009). Source: U.S. (2017a, b, c)

U.S. (2017a, b, c). In order to smooth out yearly fluctuations and country-wide shocks, we consider averages of five years before the disaster and five years after the disaster and compute the percentage change for the most affected US state relative to the US average. Except for one outlier, we observe a strong positive association between growth in households’ durable goods spending and per capita GDP growth.²

We checked the robustness of this result by restricting the time horizon to ±3 years around the disaster instead of ±5 years and arrived at basically the same positive association between growth of durable goods purchases and regional GDP growth. These results corroborate our proposed mechanism: If a disaster destroys mainly durable goods, households try to replace them quickly and supply more labor. If the regional capital stock remains intact (or, more generally was significantly less damaged than durable goods), then the increased labor supply produces more regional output than before the disaster. As a result, both durable goods expenditure and GDP are higher after the disaster. With the mechanism at work, we expect the positive impact on GDP to increase in the change of expenditure for durable goods. This is what we find in the data. The positive association visible in Fig. 1 is thus supportive of our mechanism.

Finally, we discuss evidence that disasters destroying physical capital and durable goods at the same time exert no effect on GDP when the negative and positive effects on GDP counterbalance each other. Fisker (2012) studies the spatial effect of earthquakes at the pixel level whereby land area is subdivided in 1 x 1 latitude-longitude squares (on average a size of 6832 square kilometers). The study shows that in the impact region, earthquakes affect GDP negatively, whereas GDP increases in the surrounding areas in the five years after a disaster.

² The slope of the regression line is 1.73 and the $R^2$ (omitting the outlier) is 0.73. The outlier is the Washington flood which mainly affected Oregon at the time of the Great Recession. It is explained by the fact that GDP per capita hardly declined in Oregon during the Great Recession. As a result Oregon experienced extraordinary high GDP in relation to the US. average, which confounds the assessment of the impact of the flood.
In many cases, both effects cancel each other out such that there is no impact on GDP at the country level.3

The interpretation of these findings in the light of our model is that earthquakes destroy physical capital, infrastructure and durable goods, such that the positive and negative effects are only visible at the regional level and counterbalance each other at the country level. The destructive force of the earthquake is likely to destroy capital stock mainly at the impact zone, which causes local GDP to decline. The higher labor supply in order to rebuild lost durables quickly is likely to manifest itself in higher durable goods demand and higher GDP in the impact area as well as in the neighboring areas. Fisker’s (2012) finding of the spatial distribution of the economic impact of earthquakes thus supports our claim that the positive and negative effects of disasters on GDP can counterbalance each other at the aggregate (national) level.

3 The Model

3.1 Households

The economy is populated by a continuum \((0, 1)\) of households who take prices as given, supply \(\ell\) units of labor, and experience utility from consuming nondurable goods \(c\) and durable goods \(d\) as well as from enjoying leisure \((1 - \ell)\). In order to keep the utility function general, we abstain from introducing exogenous technological growth. As well-known from the business cycle literature, introducing trend growth would entail severe restrictions on the functional form of the utility function in order to guarantee that leisure is stationary. Our variables (besides leisure) could be interpreted as being measured in terms of deviation from trend growth. In order to derive theoretical results, we have to assume that utility is additively separable between nondurable consumption, durable consumption, and leisure.4

In the quantitative part of the paper, we also investigate non-separable utility and demonstrate robustness of the main results.

Households maximize lifetime utility

\[
V = \int_0^\infty \left( u(c) + v(d) + q(1 - \ell) \right) e^{-\rho t} \, dt,
\]

where \(u, v,\) and \(q\) denote strictly concave sub-utility functions satisfying the Inada conditions and \(\rho\) is the time preference rate. To simplify the notation, we introduce \(\sigma_c, \sigma_d,\) and \(\sigma_\ell\) as the elasticity of subutility with respect to nondurable goods consumption, durable goods consumption, and leisure, respectively:

\[
\sigma_c(c) := -\frac{c u''(c)}{u'(c)} \quad \sigma_d(d) := -\frac{d v''(d)}{v'(d)} \quad \sigma_\ell(1 - \ell) := \frac{(1 - \ell) q''(1 - \ell)}{q'(1 - \ell)}.
\]

Household income is spent on nondurable consumption goods \(c\) and on durable goods \(x\). Households earn a wage \(w\) per unit of labor supplied and hold assets \(a\), on which they earn a return \(r\), which altogether implies that they face the budget constraint

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3 The only other study we are aware of which studies the effect of disasters on GDP for the impact region and surrounding areas is Strobl (2011), which shows for hurricanes a pronounced negative effect on GDP at the impact region and a positive effect on GDP for surrounding areas. However, the positive effect on surrounding areas is only statistically significant for some specifications of the econometric model.

4 Iacoviello (2005) argues that separability between nondurable and durable goods consumption is supported by empirical evidence; see also Bernanke (1984).
\[ \dot{a} = w\ell + ra - c - px, \] (3)

in which \( p \) denotes the price of durable goods purchases. We assume that a no-Ponzi-game condition for assets holds.

Durable goods depreciate at rate \( \delta_d \); hence, the stock of durables evolves according to

\[ \dot{d} = x - \delta_d d, \] (4)

with \( x \geq 0 \). Households choose \( c, \ell, a \) and \( x \) to maximize (1) subject to (3) and (4), and the initial conditions \( a(0) = a_0 \) and \( d(0) = d_0 \). The first order conditions are

\[ u'(c) = \lambda, \] (5)
\[ \mu = p\lambda, \] (6)
\[ \lambda w = q'(1 - \ell), \] (7)
\[ \dot{\lambda} = \lambda \rho - \lambda r, \] (8)
\[ \dot{\mu} = \mu \rho - v'(d) + \mu \delta_d \] (9)

\[ \lim_{t \to \infty} e^{-\rho t} \lambda a \quad \lim_{t \to \infty} e^{-\rho t} \mu d, \] (10)

where \( \lambda \) denotes the shadow price of one unit of financial assets and \( \mu \) denotes the shadow price of one unit of durable goods. From the first order conditions we derive the Euler equation for consumption and a relation equating the wage rate with the marginal rate of substitution between consumption of nondurables and leisure:

\[ \frac{\dot{c}}{c} = \frac{r - \rho}{\sigma_c}, \] (11)
\[ w = \frac{q'(1 - \ell)}{u'(c)}. \] (12)

### 3.2 Durable Goods Producing Firms

There exists a continuum \((0, 1)\) of firms producing durable goods. These firms convert units of final goods into units of durable goods. Following the DSGE literature, we assume that firms face convex adjustment costs depending on the amount of durables they produce per unit of time. These costs can be understood as, for example, arising in terms of additional planning costs when sequential tasks have to be performed in a tight time frame, or when there is inefficient labor input due to fatigue during overtime hours. Since such costs arise when investment and thus the workload is especially high, they explain why marginal costs are increasing in investment per unit of time.

The empirical literature on capital and investment adjustment costs has identified costs arising at the plant level if firms adjust the capital stock or investment (see e.g. Cooper and Haltiwanger 2006). Similar costs are likely to emerge for firms in the durable goods producing industry. In order to keep the analysis general, we assume that the total costs of producing \( x \) units of durables sum up to \( x + \psi(x) \) with a strictly convex function \( \psi \) satisfying \( \psi(0) = 0 \) and \( \psi'(0) = 0 \). For reasons of analytical tractability we assume that costs depend only on investment. Our quantitative results are robust against alternative specifications with reasonable parametrization of adjustment costs.
Total firm revenue equals $p_x$. Free entry into durable goods production implies that firms sell $x$ at unit costs:

$$p = 1 + \frac{\psi(x)}{x}. \quad (13)$$

Differentiating (13) with respect to time and using (5)–(9), we obtain the law of motion for durable goods investment as

$$\frac{\dot{x}}{x} = \left(\psi'(x) - \frac{\psi(x)}{x}\right)^{-1} \left[ p(r + \delta_d) - \frac{v'(d)}{u'(c)}\right]. \quad (14)$$

### 3.3 Final Goods Producing Firms

The economy is populated by a continuum $(0, 1)$ of firms producing final goods. Final goods are used as nondurable consumption goods, for durable goods investment, and for investment in firm capital. Each firm employs capital $k$ and labor $\ell$ to produce final output $y = Af(k, \ell)$, in which $A$ denotes total factor productivity and $f(k, \ell)$ is a neoclassical production function with positive and diminishing marginal returns. Firm capital depreciates at rate $\delta_k$. Firms have to pay adjustment costs to install capital, but we allow for the corner case of zero adjustment costs. We assume that adjustment costs $\phi(i/k)$ are convex with respect to the investment-capital ratio and we normalize adjustment costs and marginal adjustment costs to zero at the steady state. This means that adjustment costs $\phi(i/k)$ satisfy

$$\phi(\delta_k) = 0, \quad \phi'(\delta_k) = 0, \quad (15)$$

and, if $\phi \neq 0$,

$$\phi'(\cdot) > 0, \quad 2\phi'(\cdot) + \frac{i}{k\phi''(\cdot)} > 0. \quad (16)$$

The convexity of adjustment costs guarantees that an interior solution of the firms’ maximization problem exists. With these assumptions we follow the traditional literature on convex adjustment costs (e.g. Cooper and Haltiwanger 2006). For the quantitative analysis it is important to have some form of adjustment costs in order to prevent the spontaneous recovery of the capital stock after a disaster. Our main qualitative result, however, is independent from adjustment costs. In the next section we exploit this feature by setting $\phi = 0$, which allows us to focus on the wealth and employment effects of disasters.

Firms choose investment, $i$, and employment, $\ell$ to maximize

$$\int_0^\infty \left[ Af(k, \ell) - w\ell - i - i\phi\left(\frac{i}{k}\right)\right] e^{-\int_0^t r(s) ds} dt \quad (17)$$

subject to

$$\dot{k} = i - \delta_k k. \quad (18)$$

The first order conditions are:

$$w = \frac{\partial Af(k, \ell)}{\partial \ell} \quad (19)$$

$$q = 1 + \phi\left(\frac{i}{k}\right) + \left(\frac{i}{k}\right)\phi'\left(\frac{i}{k}\right) \quad (20)$$

$$\dot{q} = (r + \delta_k)q - \frac{\partial Af(k, \ell)}{\partial k} - \left(\frac{i}{k}\right)^2 \phi'\left(\frac{i}{k}\right). \quad (21)$$
with multiplier $q$. If $\phi \equiv 0$ these equation collapse to

$$
\begin{align*}
    w &= \frac{\partial Af(k, \ell)}{\partial \ell} \\
    r &= \frac{\partial Af(k, \ell)}{\partial k} - \delta_k .
\end{align*}
$$

(22) (23)

4 The Small Open Economy

In a small open economy, firm capital adjusts via international capital movements and is independent from the savings decision of domestic households. We thus focus the disaster analysis of this section on the effects originating from destruction of durable goods. For this purpose, we assume that the economy rests at a steady state before it is hit by a natural disaster. In order to focus on wealth and employment effects and to allow for a discussion by phase diagram analysis we set, for now, $\phi \equiv 0$. Because of perfect capital mobility and zero adjustment costs firms can borrow at the world interest rate $\bar{r}$, $r = \bar{r}$. This means that the world interest rate pins down the domestic capital labor ratio [Eq. (23)] and the domestic wage rate to $w = \bar{w}$ [Eq. (22)]. In order to further simplify the formal analysis, we assume that $\bar{r} = \rho$ such that households prefer a constant time profile of consumption and labor supply, $\dot{c} = \dot{\ell} = 0$ [from Eqs. (11) and (12)]. The demand for nondurable goods and durable goods as well as household labor supply is determined by the intertemporal budget constraint. This means that any shock or new information affecting the intertemporal budget constraint also affects the optimal level of $c$ and $\ell$. The implied dynamics of durable goods investment is then given by Eqs. (4) and (14).

To analyze the households’ intertemporal budget constraint we have to specify domestic households’ asset composition. We assume that households own the entire domestic capital stock such that

$$
a = k + b ,
$$

(24)

with $b$ denoting the net international investment position, i.e. the net asset position vis a vis the rest of the world. When domestic firms adjust their capital stock, domestic households, ceteris paribus, do not change their level of assets $a$ but restructure their portfolio such that they supply the demanded stock of capital and adjust $b$ residually.

In order to explain how a disaster destroying durable goods affects GDP, we begin by showing that the destruction of durables entails a negative wealth effect. Households respond to the wealth effect by consuming fewer nondurables and durables and by supplying more labor. Higher labor supply then lifts GDP above the pre-shock level.

Integrating Eq. (3) provides the households’ intertemporal budget constraint,

$$
\int_0^\infty ce^{-rt} dt = \ell \int_0^\infty \bar{w}e^{-\bar{r}t} dt - \int_0^\infty p(x)xe^{-rt} dt + a_0 .
$$

(25)

Using the fact that $c$ and $\ell$ are constant, the budget constraint simplifies to

$$
\frac{c}{\bar{r}} = \frac{\ell \bar{w}}{\bar{r}} - \int_0^\infty p(x)xe^{-\bar{r}t} dt + a_0 .
$$

(26)

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Finally, substituting \( w = v'(1 - \ell)/u'(c) \), we obtain
\[
\frac{(u')^{-1} \left( \frac{q'(1-\ell)}{w} \right)}{r} - \frac{\ell \bar{w}}{r} = a_0 - \int_0^\infty p(x)x e^{-\bar{r}t} dt.
\] (27)

Notice that the left-hand side of (27) depends negatively on \( \ell \) since \( d \left( u'(\cdot)^{-1}/d(\cdot) < 0 \right. \). This means that households supply more labor when they experience a negative wealth effect such that the right-hand side of (27) decreases.

We next show that an economy initially situated at a steady state experiences indeed a negative wealth effect when it is exposed to a disaster that destroys part of \( d \). For that purpose we define the net present value of durable goods investments as
\[
X := \int_0^\infty p(x)x e^{-\bar{r}t} dt = \int_0^\infty x \left( 1 + \frac{\psi(x)}{x} \right) e^{-\bar{r}t} dt.
\] (28)

Intuitively, a disaster that destroys parts of \( d \), raises \( X \), because rebuilding the stock of \( d \) requires higher temporary investments \( x \), which raises the net present value of future investments. In order to verify this claim we focus on the dynamics of \( d \) and \( x \) summarized by
\[
\dot{d} = x - \delta_d d,
\] (29)
\[
\frac{\dot{x}}{x} = \left( \psi'(x) - \frac{\psi(x)}{x} \right)^{-1} \left[ \left( 1 + \frac{\psi(x)}{x} \right) (r + \delta_d) - \frac{v'(d)}{u'(c)} \right],
\] (30)
and \( d(0) = d_0 \). The steady state of the subsystem (29) and (30) is given by \( x = \delta_d d \) and \( (1 + \psi(x)/x) (r + \delta_d) = v'(d)/u'(c) \). Notice that the steady state of the subsystem depends on \( c \) and that \( c \) is determined in conjunction with \( x \) by the intertemporal budget constraint (27) and the labor supply Eq. (12). This means that the steady state itself depends on the evolution of the dynamic system towards the steady state. In other words, the steady state of the dynamic subsystem (29) and (30) depends on the initial situation \( (c_0, x_0) \).\(^5\)

In order to demonstrate that adjustment dynamics towards the steady state are unique, we construct a phase diagram, taking \( c \) as given and keeping in mind that \( c \) depends on \( X \) and therefore on the adjustment path of \( x \). The panel on the left-hand side of Fig. 2 shows the phase diagram with adjustment dynamics towards the steady state. The phase diagram is constructed by first noting that the \( \dot{d} = 0 \) isocline is a ray with slope \( \delta_d \) starting at the origin (from \( x^* = \delta_d d^* \)). Above the line, \( \dot{d} \) is positive; and below the line, \( \dot{d} \) is negative. The \( \dot{x} = 0 \) isocline is downward sloping and intersects the \( \dot{d} \) axis at \( d = (u')^{-1} (u'(c)(\bar{r} + \delta_d)) \). On the right-hand side of the line, \( \dot{x} \) is positive; and on the left hand side, \( \dot{x} \) is negative. The slopes of the two isoclines have opposite signs, implying that the isoclines intersect exactly once. In conclusion, the steady state is saddlepath-stable. A higher value of \( c \) (lower \( X \)) shifts the \( \dot{x} = 0 \) isocline upwards; hence, the steady state value of \( d \) increases. The stable saddlepath towards the steady state is downward sloping. In “Appendix” A we formally derive that a unique and saddle-point stable steady state exists for subsystem (29) and (30).

In comparison with conventional growth theory, the usual argument for uniqueness of adjustment dynamics is slightly modified. To see this, consider an economy starting somewhere below the stable saddlepath. Following the arrows of motion, the economy would always remain below the saddlepath such that aggregate \( X \) would also be lower. Then, from the intertemporal budget constraint (27), consumption \( c \) must be higher. This in turn means

\(^5\) A similar type of phase diagram for the analysis of dynamic subsystems has been popularized in growth economics by Galor and Weil (2000).
that the $\dot{x} = 0$ isocline, and thus the steady state, shifts upwards. An economy starting below the stable saddlepath would thus never arrive at the steady state because $x$ is below the stable saddlepath everywhere during the transition and, secondly, because this very phenomenon shifts the steady state even further upwards. Analogously an economy starting above the saddlepath would never reach the steady state.\footnote{The local uniqueness of the saddlepath can also be proven by analyzing the full dynamic system of $c$, $x$, $d$, and $a$. It can be shown that of the four Eigenvalues of the Jacobian matrix two are positive, one is negative, and one is zero. This indicates that the stable saddlepath is unique and that the steady state to which the economy converges depends on the initial conditions ($a(0) = a_0$ and $d(0) = d_0$). We thank Franz X. Hof for this proof. The proof is available upon request.} This reasoning can be exploited to arrive at the following conclusion.

**Lemma 1** If an economy rests at a steady state and durable goods ($d$) are destroyed, aggregate expenditure on durable goods ($X$) increases compared to the pre-shock steady-state level.

**Proof** The lemma is proved by contradiction. The counterfactual phase diagram is shown in the panel on the right-hand side of Fig. 2. Assume that the destruction of durables $d$ reduces aggregate durables expenditure $X$. In this case, Eqs. (27) and (12) show that $c$ would increase; thus the $\dot{x} = 0$ isocline would shift upwards. This would increase the steady state value of $d$. However, along the adjustment path, $x$ is strictly larger than its former steady state because the stable saddlepath is downward sloping, $x(t) > x^{*}_{old}$, implying increasing aggregate expenditure $X$. In other words, reducing $X$ in response to lower $d$ would lead to a contradiction. If $X$ would remain constant, this would lead to a contradiction in an analogous way. In conclusion, after a destruction of $d$, $X$ rises compared to its original steady-state level. \hfill $\square$

In short, the actual adjustment dynamics triggered by a natural disaster destroying $d$ are shown in Fig. 3. Notice that along the adjustment path $x$ is larger compared to the old steady state for an initial period $[0, T]$. During the time interval $(T, \infty)$ $x$ is smaller than $x^{*}_{old}$. Yet due to discounting of future expenditures and higher adjustment costs in the initial periods, $X$ increases in net terms. This leads to the following result.

Fig. 2 Phase diagram. Left panel: phase diagram with stable saddlepath. Right panel: phase diagram used for proof of Lemma 1

\[ x^* = \delta d^* \]

\[ d^* = 0 \]

\[ x^{*}_{old} \]

\[ d^{*}_{old} \]
**Proposition 1** If an economy rests at a steady state and durable goods \( (d) \) are destroyed, only parts of the stock of \( d \) are rebuilt. The resulting new steady-state level of \( d \) is lower compared to pre-shock level.

*Proof* Inspecting the adjustment dynamics derived in Fig. 3 confirms that the after-shock steady-state level of \( d \) lies below the pre-shock steady-state level.

The result implies that without trend growth, an economy never completely rebuilds the stock of durables destroyed by a disaster. If there is trend growth, \( d \) would grow at the steady state and the post-disaster growth rate of \( d \) would be higher than the pre-shock rate. However, the level of \( d \) would be lower compared to an economy not experiencing the disaster and growing along the balanced growth path. The reason for the permanently lower level of durable goods is the negative wealth effect. Households respond to the diminished wealth by reducing their consumption of nondurable goods, consumption of durable goods, and leisure. This leads to our next result.

**Proposition 2** Aggregate welfare falls below its pre-shock level if durable goods are destroyed in an economy resting at a steady state.

*Proof* According to Proposition 1, the level of durable goods after the disaster falls permanently below the pre-shock level. From Lemma 1, we conclude that consumption of nondurable goods is also permanently lower. Finally, we conclude from Eq. (27) that labor supply increases. Since instantaneous utility from all three components is strictly below pre-shock level, the lifetime utility of households, i.e. aggregate welfare, is below the pre-shock level as well.

Finally, we show that, although aggregate welfare is affected negatively, output and output growth increase in response to the disaster, and we derive conditions under which GDP also responds positively.
Proposition 3 If durable goods are destroyed in an economy resting at a steady state, then aggregate output per capita increases permanently above the pre-shock level. Hence, output growth in the aftermath of the disaster is positive.

Proof If \( d \) is destroyed, consumption of nondurable goods decreases [see Eq. (12)] and labor supply increases [see Eq. (27)]. Higher labor supply triggers capital inflows from the rest of the world until the capital labor ratio reaches its pre-shock level and the domestic interest rate equals the world interest rate. Higher labor supply in conjunction with higher capital stock implies higher aggregate output per capita.

In an open economy, GDP differs from GNP by factor income received from abroad such that, in our case, \( GNP = GDP + rb \). GNP is positively influenced by increasing GDP and negatively by a declining net foreign asset position \( b \). The net foreign asset position deteriorates because the capital stock of firms increases as a response to higher labor supply and households restructure their portfolio to serve the higher domestic capital demand by reducing \( b \). Moreover, expenditure on durable goods is higher in the initial years after the disaster compared to expenditure at the steady state. This means that the savings rate is negative in the aftermath of a disaster such that \( a \), and thus \( b \), declines in the years following a disaster. Since GDP increases and \( b \) declines, the response of GNP is undetermined and depends on households’ preferences. We illustrate this fact by focussing on two extreme cases. The first case assumes inelastic labor supply. This assumption closes down the labor supply channel of disasters on GDP. However, households still raise their expenditure on durable goods in the aftermath of the disaster and, hence, \( b \) declines. The impact of a disaster on GNP would thus be negative.

The second case assumes infinitely elastic labor supply. In this case, nondurable consumption does not decline as a response to the disaster because households raise their labor supply by so much that the negative wealth effect is fully compensated by higher labor income (see Strulik and Trimborn 2017, for a formal proof). This implies that the stock of destroyed durables is completely rebuild in the long run. Evaluating Eq. (26) shows that the increase of labor income in net present value terms is equal to the decline of durable goods expenditure in net present value terms, i.e. \( \Delta \ell \cdot \bar{w}/\bar{r} = \Delta X \). We derive the impact on households’ assets at the new steady state by evaluating Eq. (26) again, now at the new steady state. There, \( \bar{c} \) and \( X \) are equal to their old steady state values, whereas labor income is higher. Assets \( a \), at the new steady state, are determined residually, i.e. they have to be lower exactly by excess labor income in order to balance the equation. This means that at the new steady state households’ assets are reduced by the net present value of reconstruction costs. Comparing the old and the new steady state, we compute the change in the net foreign asset position as

\[
\Delta b = \Delta a - \Delta k = -\Delta X - \Delta k = -\Delta \ell \cdot \bar{w}/\bar{r} - \Delta k.
\]

Using this result, the response of GNP at the new steady state is obtained as

\[
\Delta GNP^* = \Delta \ell w + \Delta kr + \bar{r} \Delta b = \Delta \ell w + \Delta kr - \Delta \ell \cdot \bar{w} - \bar{r} \Delta k = 0.
\]

To assess the response of GNP on impact recall that the decline in \( b \) fades in over time. Hence, GNP is higher on impact, compared to the new steady state, then converges towards the old steady state as time proceeds.
5 The Closed Economy Case

5.1 Setup of the Model

The closed economy case can be best understood as a standard neoclassical growth model augmented by a durable goods producing sector and variable labor supply. In a closed economy, households save only in terms of domestic capital such that \( a = k \). The feature of diminishing marginal returns to capital provides a unique steady state. \(^7\)

The evolution of the economy is described by the household’s first order condition, the durable good producing firms’ first order conditions, and the final good producing firm’s first order condition. In addition, equilibrium on the goods market requires that output is used up for nondurable consumption, physical capital investment, durable goods investment, depreciation, and adjustment costs for capital and durable goods investment. For convenience, we summarize below the equations describing the closed economy:

\[
\dot{k} = i - \delta_k k \\
\dot{d} = x - \delta_d d \\
\dot{c} = \frac{r - \rho}{\sigma_c} \\
\dot{x} = \left( \psi'(x) - \frac{\psi(x)}{x} \right)^{-1} \left[ p(r + \delta_d) - \frac{u'(d)}{u'(c)} \right] \\
\dot{q} = (r + \delta_k)q - \frac{\partial A f(k, \ell)}{\partial k} - \left( \frac{i}{k} \right)^2 \phi'(\frac{i}{k}) \\
q = 1 + \phi \left( \frac{i}{k} \right) + \left( \frac{i}{k} \right) \phi'(\frac{i}{k}) \\
A f(k, \ell) = \delta_k k + x + \psi(x) + c + i + i \phi \left( \frac{i}{k} \right) \\
\frac{\partial A f(k, \ell)}{\partial \ell} = \frac{q'(1 - \ell)}{u'(c)}.
\]

5.2 Effect of Disasters on GDP: Intuition

To illustrate our argument, we distinguish between two polar types of disasters. The first type destroys only durable goods while the second type destroys only productive capital. In reality, of course, disasters usually destroy both \( d \) and \( k \). Real disasters can be conceptualized as a mix of the two polar cases. In the quantitative section, we first discuss results for the two polar types of disasters and then investigate the impact of “mixed disasters”.

We begin the analysis again by inspecting the intertemporal budget constraint. Integrating (3) and inserting \( a_0 = k_0 \), we obtain

\[
\int_0^\infty e^{-\int_0^s r(u)\,du} \, ds = k_0, \quad \int_0^\infty w \ell e^{-\int_0^s r(u)\,du} \, ds = \int_0^\infty p(x) x e^{-\int_0^s r(u)\,du} \, ds.
\]

The intertemporal budget constraint differs from the open economy case (Eq. 27) mainly because the wage rate \( w \) and the interest rate \( r \) are now varying over time. A damaged stock

\(^7\) In the “Appendix”, we show that the dynamic system (33)–(40) has a unique steady state. We also checked by numerically evaluating the eigenvalues that adjustment dynamics are unique for the relevant range of parameter values.
of productive capital entails temporarily lower wages and higher interest rates and these changing factor prices impinge on household wealth. As demonstrated below, these “factor price effects” are quantitatively of second order compared to the wealth effect originating from the loss of productive capital or durables.

We start by analyzing a $d$-shock. As for the small open economy, destroyed durables entail reconstruction costs such that the present value of durable goods investments $\int_0^\infty p(x)xe^{-\int_0^s r(u)du}ds$ increases. This, in turn, implies lower household wealth. Households respond to the reduced wealth by lowering consumption of nondurable goods and by supplying more labor. In the quantitative section below we show that on top of the wealth effect there exists an intertemporal substitution effect that amplifies the response of employment. Since international capital markets are no longer available to smooth consumption, households are motivated to raise labor supply even further in the initial years after the disaster in order to mitigate the drop in consumption. At the same time, high reconstruction costs also raise labor demand. Productive capital, by assumption, was not affected by the disaster, which means that higher employment lifts output above its pre-shock level.

The impact of a disaster destroying productive capital can be investigated analogously. The $k$-shock reduces $k_0$ on the right-hand side of Eq. (41) and thus entails a negative wealth effect as well. Households respond by consuming less nondurable goods, by reducing durable goods investment, and by supplying more labor. The reason for this joint response lies in the fact that nondurables, durables, and leisure are normal goods such that the demand for all three components shifts in the same direction after a wealth shock. In contrast to the $d$-shock, higher labor supply is not sufficient to lift output above the steady-state level. For reasonable parameter values, the negative impact of the lower level of capital stock after the shock is the dominant force on output. This means that we observe the conventional “neoclassical” adjustment dynamics: the economy starts at a lower level of output and converges towards the steady state from below.

6 Quantitative Analysis

6.1 Numerical Specification of the Model

In order to parameterize the model, we need to specify the form of the utility function and the production technology. We assume that households face an isoelastic utility function

$$\int_0^\infty \left[ \frac{c^{1-\sigma_c} - 1}{1 - \sigma_c} + \beta \frac{d^{1-\sigma_d} - 1}{1 - \sigma_d} + \eta \frac{(1 - \ell)^{1-\sigma_\ell} - 1}{1 - \sigma_\ell} \right] \cdot e^{-\rho t} dt$$

in which $\beta$ and $\eta$ denote the weights of durable goods and leisure, respectively. In Sect. 6.3, we relax the assumption of separability between nondurable and durable goods. Firms are assumed to produce according to the Cobb-Douglas production technology $y = Ak^\alpha \ell^{1-\alpha}$, in which $\alpha$ denotes the elasticity of output with respect to capital. Adjustment costs for durable goods investment and capital investment are quadratic, as it is often assumed in the DSGE literature (see e.g. Christiano et al. 2011), i.e. $\psi(x) = \gamma x^2$ and $\phi(i/k) = \kappa (i/k - \delta_k)^2$. We normalize the cost parameters $\gamma$ and $\kappa$ to unity.

For the benchmark case we take the values of $\alpha, r^*, \ell^*$, and the Frisch elasticity of labor supply from our calibration of the neoclassical growth model for the U.S. economy (Strulik and Trimborn 2012). For depreciation of physical capital we take the average depreciation rates measured for the U.S. between 1948 and 2008 (Davis and Heathcote 2005). Parameter $\eta$
Table 1 Parameter values: benchmark model

| Parameter       | Value     |
|-----------------|-----------|
| $A$             | 1         |
| $\alpha$        | 0.38      |
| $\delta_k$      | 0.058     |
| $\delta_d$      | 0.18      |
| $r^*$           | 0.038     |
| $(\rho)$        | 0.038     |
| $\gamma$        | 1         |
| $\kappa$        | 1         |
| $\ell^*$        | 0.25      |
| $(\eta)$        | 10.7      |
| Frisch          | 1         |
| $(\sigma_\ell)$| 3         |
| $\sigma_c$      | 2         |
| $\sigma_d$      | 2         |
| $\beta$         | 4.39      |

Notation in parenthesis indicates implied values.

is set in order to match steady-state labor supply $\ell^*$, and $\rho$ is set in order to fit the steady-state interest rate to $r^*$. For given $\ell^* = 0.25$ and a given Frisch elasticity of unity, we obtain $\sigma_\ell = 3$. The inverse of the intertemporal elasticity of substitution for consumption of durables and nondurables, respectively, is set to 2, based on Ogaki and Reinhart (1998).

We set $\beta$ in order to match the expenditure ratio of nondurable to durable goods, according to the US Consumption Expenditure Survey of 2014 (Bureau of Labor Statistics 2014). For durable goods we have only estimates of depreciation rates when they are treated as investment goods (see House and Shapiro 2008). These estimates range from 0.3 for communication equipment, software, computers and peripheral equipment, to 0.165 for cars, and to 0.06 for boats. We take a weighted average of the depreciation rate for all items, which provides the estimate $\delta_d = 0.18$. The numerical specification of the benchmark model is summarized in Table 1.

6.2 Numerical Experiments

Quantitative results are calculated by employing the relaxation algorithm (Trimborn et al. 2008). The solution method calculates adjustment dynamics of non-linear models and provides the exact solution, up to a user-specified error. It is thus a suitable tool to investigate natural disasters, i.e. big shocks that drive the economy far away from the steady state. We employ a recently developed numerical method to ensure that non-negativity constraints on capital investment and durable goods investment hold during the adjustment process (Trimborn 2013).

Because we already showed analytically that disasters destroying durable goods exert an unambiguously positive effect on output in the small open economy case, we focus on the closed economy case and investigate three different types of disasters: a $d$-disaster destroying only durable goods, a $k$-disaster destroying only productive capital, and a “mixed disaster” destroying parts of both stocks. We assume that the economy rests at the steady state and that the disaster comes unanticipated. We normalize the size of disasters such that the value of assets destroyed is equal in all three cases. Because the capital stock at the steady state is about twice as large as the value of durables this implies that a shock destroys either 10% of the capital stock or 20% of the stock of durables, or—in case of a mixed disaster—3% and 15% of capital and durables, respectively.

Figure 4 shows the impulse responses following a destruction of $d$ by 20% of the steady-state level. As a reaction to the disaster, households increase durable goods purchases above the steady-state level in order to rebuild the damaged stock of durables. The resulting negative wealth effect causes households to reduce nondurable consumption and to increase labor supply. Higher labor supply in the aftermath of the disaster lifts output above steady-state level. Later, when the economy recovers and the damaged stock of durables is rebuilt, economic aggregates return to their pre-shock steady-state levels.

There exists, on top of the wealth effect, an intertemporal substitution effect, which amplifies the positive response of labor supply and output. Due to their damaged durables, households experience a high marginal utility from durable goods consumption, which
Fig. 4  Natural disasters: destruction of durable goods. Impulse responses to the destruction of durable goods by 20%. The panel shows the response of capital \((k)\), durable goods \((d)\), durable goods investment \((x)\), nondurable consumption \((c)\), labor supply \((\ell)\), and GDP

induces them to rebuild their stock of durables quickly and to incur high costs of durable goods investments. Since households cannot borrow on international capital markets, resources are scarce in the aftermath of a disaster. In order to free resources, households reduce capital investment and consumption. Then, in order to mitigate the drop in consumption, households further increase their labor supply. As a consequence, output in the initial periods after the disaster rises even further, beyond the increase triggered by the wealth effect.

As a side effect, lower investment in productive capital reduces the capital stock. Only after about three years—when about two thirds of the durable goods have been reconstructed—investment in capital is higher than depreciation and the capital stock returns to its steady-state level from below.

In our numerical simulations it turns out that as long as the Frisch elasticity of labor supply is positive, the initial response of labor supply and hence of output is positive. Our numerical analysis also reveals that the size of the intertemporal elasticity of substitution in durable and non-durable consumption has a large impact on the quantitative response of output. As a rule, the positive response of output is stronger when the intertemporal elasticity of substitution is low (high \(\sigma_c\) and \(\sigma_d\)).

Although the disaster has a positive effect on GDP, the effect on welfare is clearly negative. Households experience lower utility from durable goods as a direct result of the disaster. Furthermore, they experience lower levels of nondurable consumption and leisure (as a result of the intertemporal substitution effect and the wealth effect). Hence, all three components of instantaneous utility, i.e. \(u(\cdot)\), \(v(\cdot)\), and \(q(\cdot)\), are affected negatively. In order to make welfare losses comparable we measure them in consumption equivalents of nondurable goods. In the benchmark case the accumulated welfare loss amounts to 4.1% compared to the pre-shock steady-state welfare level. This number means that a household living in the economy struck by the disaster suffers the same welfare loss as a household permanently losing 4.1% of nondurable consumption. Income and welfare effects of the disaster are summarized in Table 2.

We next turn to a shock that destroys physical capital \(k\). In Fig. 5, we show the impulse responses caused by a reduction of \(k\) by 10%. Consumption and labor supply respond in the same way as for the \(d\)-shock. On impact, households consume less nondurable goods and supply more labor because of the negative wealth effect. Similar to the \(d\)-shock, there is also an
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Table 2  GDP and welfare effects of natural disasters

|                      | $d$-disaster (%) | $k$-disaster (%) | Mixed-disaster (%) |
|----------------------|------------------|------------------|--------------------|
| Separable utility    | $\Delta y = +0.4$ | $\Delta y = -1.7$ | $\Delta y = 0.00$  |
|                      | $\Delta W = -4.1$ | $\Delta W = -3.5$ | $\Delta W = -3.9$  |
| Non-separable utility| $\Delta y = +0.7$ | $\Delta y = -1.7$ | $\Delta y = -0.9$  |
|                      | $\Delta W = -4.0$ | $\Delta W = -3.5$ | $\Delta W = -3.9$  |

$\Delta y$ denotes the average percentage deviation of output compared to the pre-shock level during the first three years, $\Delta W$ denotes the percentage deviation of welfare compared to the pre-shock steady-state level, measured in nondurable consumption equivalents. A $d$-disaster is a 20% reduction of durable goods compared to the steady-state level, a $k$-disaster is a 10% reduction of productive capital, and a mixed disaster is a 15% reduction of durables and a 3% reduction of productive capital.

![Graph](image)

Fig. 5  Natural disasters: destruction of productive capital. Impulse responses to the destruction of productive capital by 10%

Intertemporal substitution effect at work. Since high capital investments are needed in order to rebuild the capital stock, resources are scarce during initial periods. Hence, households react by reducing durable goods investments, nondurable consumption and increasing labor supply. The intertemporal substitution effect works on top of the wealth effect and thus amplifies labor supply in the aftermath of the disaster.

Although labor supply is higher compared to the pre-shock level in the initial periods, output decreases after the $k$-shock. The effect of lower productive capital on output dominates. As already pointed out, this is not a general result but holds for reasonable parameterizations of the neoclassical growth model. Only when the Frisch elasticity of labor supply is infinite and the share of capital in production is implausibly low, output would respond positively to a $k$-shock (see Strulik and Trimborn 2015).

For welfare, the intuition developed in conjunction with the standard neoclassical growth model holds for the $k$-disaster as well. A lower capital stock unambiguously causes welfare to decline. This can be seen by inspecting the time path of durables ($d$), nondurable consumption ($c$), and labor supply ($l$). As a response to the negative wealth effect, households enjoy lower levels of nondurable consumption and leisure. In addition, temporarily lower durable goods investment reduces the stock of durables. Since all three components of utility are affected negatively, overall utility is lower. We calculate a welfare loss of 3.5% measured in consumption equivalents.
Finally, we investigate a shock that destroys both capital and durable goods simultaneously. This opens up the possibility that output remains unaffected in the aftermath of a disaster, because the positive effect through higher labor supply and the negative effect through lower productive capital balance each other. For our benchmark calibration, a disaster destroying 15% of durables and 3% of productive capital has a negligible effect on output, as shown in Fig. 6.

In our example, the effects of destruction of productive capital and durable goods roughly balance each other. Output per capita and GDP per capita remain largely unaffected. Nevertheless, a “GDP-neutral” disaster has substantial effects on other economic aggregates and on welfare because all three components of welfare are affected negatively. Households enjoy less durable goods (as a direct result of the disaster) as well as lower consumption of nondurable goods and lower leisure (as a result of the intertemporal substitution effect and the wealth effect). As a result, the benchmark “mixed” disaster causes aggregate welfare to decline by 3.9%.

6.3 Non-separable Utility

The assumption of a separable utility function simplifies the analysis and thus most of the related literature assumes that utility experienced from consumption of durable and nondurable goods is separable. The study by Ogaki and Reinhart (1998), however, suggests that utility between nondurable and durable consumption is non-separable. In order to demonstrate robustness of our main results with respect to non-separability, we adopt the utility function suggested by Ogaki and Reinhart (1998) and extend it with utility experienced from leisure. This means that households maximize

$$
\int_0^\infty \left( \frac{e^{1-\epsilon} + \beta d^{1-\epsilon}}{1 - \sigma} \right)^{1-\sigma} \left( \frac{1 - \epsilon}{1 - \sigma} + \eta \frac{(1 - \epsilon)^{1-\sigma\epsilon} - 1}{1 - \sigma\ell} \right) e^{-\rho t} dt
$$

subject to the budget constraints (3) and (4). We adopt the parameter estimates from Ogaki and Reinhart for $\epsilon$ and $\sigma$, i.e. $\epsilon = 1.167$ and $\sigma = 2.2$, and we adjust $\beta$ such that the ratio of nondurable to durable goods expenditure matches the data from the US Consumption
Expenditure Survey of 2014. All other parameter values are taken from our benchmark calibration.

The second part of Table 2 summarizes the GDP and welfare results for the three different types of disasters under non-separable utility. We observe only mild changes compared to the separable utility case. Given the new utility function (and everything else from the benchmark model), the mixed disaster has a mildly negative impact on GDP. By adjusting the degree of destruction of durable goods and capital stock we could, of course, produce a mixed disaster of exactly zero impact. Altogether we conclude robustness of our results with respect to the assumption of non-separable utility.

7 Residential Housing

Apart from physical capital and durable goods, disasters can also destroy residential housing. We have to discuss effects on residential housing separately because houses depreciate at a much lower rate than durable goods and because houses are treated differently from durable goods in the national accounting statistics (see below). To test the robustness of our results and to allow for disasters destroying residential housing in addition to other assets we extend the baseline model by a residential housing sector. Everything else from the benchmark model remains the same.

7.1 Model Setup

In the extended model, households derive utility from nondurable consumption, durable consumption, residential housing services \( h \), and leisure, and maximize

\[
V = \int_0^\infty (u(c) + v(d) + v_h(h) + q(1 - \ell)) \cdot e^{-\rho t} dt,
\]

subject to

\[
\dot{h} = i_h - \delta_h h,
\]

the augmented budget constraint

\[
\dot{a} = w + ra - c - px x - p_{ih} i_h,
\]

the accumulation equation for durable goods (4), the initial conditions \( a(0) = a_0, d(0) = d_0, h(0) = h_0 \), and a no-Ponzi-game condition. The price of residential investment is denoted by \( p_h \).

Furthermore, we have now a third type of firms producing residential investment. These firms convert units of final output into residential investment \( i_h \) and face adjustment costs \( \psi_h(i_h) \), as the firms producing durable goods. Each household is assumed to engage one construction firm per unit of time and may change the contracting party at any point of time. Free entry into construction implies that firms set the price for residential investment at unit costs:

\[
p_{ih} = 1 + \frac{\psi_h(i_h)}{i_h}.
\]
We summarize the equations characterizing the evolution of the economy:

\[ \dot{k} = i - \delta_k k \]  
\[ \dot{d} = x - \delta_d d \]  
\[ \dot{h} = i_h - \delta_h h \]  
\[ \frac{\dot{c}}{c} = \frac{r - \rho}{\sigma_c} \]  
\[ \frac{\dot{x}}{x} = \left( \psi'(x) - \frac{\psi(x)}{x} \right)^{-1} \left[ p(r + \delta_d) - \frac{u'(d)}{u'(c)} \right] \]  
\[ \frac{\dot{i}_h}{i_h} = \left( \phi'(x) - \frac{\phi(i_h)}{i_h} \right)^{-1} \left[ p_{i_h}(r + \delta_h) - \frac{v'_h(d)}{u'(c)} \right] \]  
\[ \dot{q} = (r + \delta_k)q - \frac{\partial A f(k, \ell)}{\partial k} - \left( \frac{i}{k} \right)^2 \phi' \left( \frac{i}{k} \right) \]  
\[ q = 1 + \phi \left( \frac{i}{k} \right) + \left( \frac{i}{k} \right) \phi' \left( \frac{i}{k} \right) \]  
\[ A f(k, \ell) = \delta_k k + x + \psi(x) + i_h + \phi(i_h) + c + i + i \phi \left( \frac{i}{k} \right) \]  
\[ \frac{\partial A f(k, \ell)}{\partial \ell} = q'(1 - \ell) \frac{u'(c)}{u'(c)} \] .

### 7.2 Output and GDP

In most macroeconomic models, aggregate output equals GDP. Here, in a model with residential houses, we have to distinguish between these aggregates. The reason is that the System of National Accounts (SNA) requires to account for the service flow from already installed houses as part of consumption, and thus, as a part of GDP (see EC, IMF, OECD, UN & World Bank 2009, pp. 466–467). In particular, SNA states that houses leased to other households are supposed to be treated equivalently to owner-occupied houses. A newly constructed house raises output and GDP according to its construction costs. In the following years, the house contributes to GDP—but not to output—according to the rent paid by its tenant (if it is leased) or according to an imputed rent (if it is owner occupied). Houses are the only durable good from which a service flow enters GDP calculations. For example, service flows from cars used for consumption purposes are not included as part of GDP.

In terms of our model, newly constructed houses are immediately accounted for in output and GDP in terms of their construction costs. Because houses are owner-occupied in our benchmark model, we introduce an imputed rent in order to account for the contribution of housing services to GDP. In “Appendix B”, we set up an alternative model in which houses are leased to households by real estate firms. We show that the alternative setup is equivalent to the benchmark model, and that the equilibrium rental price \( p_h \) for renting one unit of \( h \) for one unit of time is equal to

\[ p_h = \frac{v'_h(d)}{u'(c)}. \]  

Intuitively, the price ratio between durable consumption goods and residential houses, \( p_h/1 \), is equal to the marginal rate of substitution between durable consumption goods and nondurable
consumption goods, \( v'_h(d)/u'(c) \). In the following, we use (58) as the imputed price for GDP accounting. Hence, GDP equals

\[
GP_{N} = y + p_h h. 
\tag{59}
\]

Notice that, without residential housing, GDP coincides with output. Taking residential housing into account, the measurement of GDP matters as well. In Eq. (59) GDP is by construction measured in terms of the numeraire, i.e. in terms of consumption goods. In order to compare our results with numbers from actual GDP accounting we convert \( GP_{N} \) into GDP measured by a weighted price index of non-durables and durables, \( GDP = GP_{N}/P \). The price index \( P \) is calculated as a weighted average from the Paasche and Laspeyres price indices using the geometric mean (Fisher index).

7.3 Calibration

We assume that households face isoelastic utility according to

\[
\int_0^\infty \left[ \frac{c^{1-\sigma_c} - 1}{1 - \sigma_c} + \beta \frac{d^{1-\sigma_d} - 1}{1 - \sigma_d} + \beta_h \frac{h^{1-\sigma_h} - 1}{1 - \sigma_h} + \eta \frac{(1 - \tau)^{1-\sigma_c} - 1}{1 - \sigma_c} \right] \cdot e^{-\rho t} dt. \tag{60}
\]

where \( \beta_h \) denotes the weight of housing in utility. We further assume that adjustment costs are quadratic, i.e. \( \phi(i_h) = \gamma_h i_h^2 \).

For depreciation of residential houses we take the average depreciation rates measured for the U.S. between 1948 and 2008 (Davis and Heathcote 2005; Eerola and Määttänen 2013), i.e. \( \delta_h = 0.015 \). We set \( \beta_h \) in order to match the share of households’ housing assets on total assets of about 0.5 in the year 2008 (see Iacoviello 2010 and Iacoviello 2011), and we reestimate \( \beta \) such that the spending share of durable goods investment and nondurable consumption match the data from the Consumption Expenditure Survey. This gives \( \beta_h = 6.0 \) and \( \beta = 4.34 \). Finally, we set the adjustment cost parameter \( \gamma_h \) equal to one. All other parameters are taken from the benchmark calibration.

7.4 Results

In the extended model, a disaster may not only destroy physical capital and durable goods, but also residential housing. However, it is unlikely that a disaster destroys residential housing and leaves durable goods intact. This would mean that the structure of houses gets damaged while the interior (e.g. furniture) remains intact. We therefore focus on three types of disasters: As before, we consider a \( d \)-disaster where only durable goods get destroyed and a \( k \)-disaster where only physical capital gets destroyed. Additionally, we consider a mixed disaster where residential housing and durable goods get destroyed. The mixed disaster offers another possibility how a disaster could be GDP-neutral. When residential houses get destroyed, the service flow from houses adding to GDP is lower in the aftermath of the disaster thus leading to the prediction of lower GDP through an accounting effect. However, as shown above, the destruction of both durables and residential houses exerts a positive impact on output, and thereby on GDP, through higher labor supply. A mixed disaster will thus be GDP-neutral when the output effect counterbalances the accounting effect. We summarize the impact of a mixed disaster destroying 15% of durable goods and 2.5% of residential houses in Fig. 7. The amount of destroyed durables and houses is chosen such that the amount of destroyed assets is the same as in the previous scenarios, and such that the resulting response of GDP is insignificant.
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Fig. 7 Natural disaster: mixed disaster in the extended model. Impulse Responses to the destruction of durable goods by 15% and residential housing of 2.5%. The panel shows the response of capital ($k$), durable goods ($d$), residential housing ($h$), durable goods investment ($x$), residential investment ($ih$), nondurable consumption ($c$), labor supply ($\ell$), imputed rents for houses ($ph$), output ($y$), and GDP.

Table 3 Impact of disaster on output, GDP, and welfare

| $d$-disaster (%) | $k$-disaster (%) | Mixed-disaster (%) |
|------------------|------------------|-------------------|
| $\Delta y = +0.35$ | $\Delta y = -2.0$ | $\Delta y = +0.58$ |
| $\Delta GDP = +0.12$ | $\Delta GDP = -1.8$ | $\Delta GDP = 0.00$ |
| $\Delta W = -4.2$ | $\Delta W = -3.2$ | $\Delta W = -3.7$ |

$\Delta y$ denotes the average percentage deviation of output compared to the pre-shock level during the first three years, $\Delta GDP$ denotes the average percentage deviation of GDP compared to the pre-shock level during the first three years, $\Delta W$ denotes the percentage deviation of welfare compared to the pre-shock steady-state level, measured in nondurable consumption equivalents. A $d$-disaster is a 20% reduction of durable goods compared to the steady-state level, a $k$-disaster is a 10% reduction of productive capital, and a mixed disaster is a 15% reduction of durables and a 2.5% reduction of residential housing.

The results for output, GDP, and welfare are summarized in Table 3. The direction of impact as well as its size for the three disasters is similar to the benchmark case (discussed in Table 2). The positive impact of the $d$—disaster on GDP is smaller than on output due to the reduced service flow from housing. For the same reason, the mixed disaster exerts a mildly positive impact on output while it leaves GDP unaffected.

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8 Conclusion

In this paper, we developed a theory that offers an explanation for the puzzling empirical finding that output and GDP in the aftermath of natural disasters are not necessarily lower than before the event, and in some cases even higher than before. We have shown that disasters destroying mainly durable goods drive output and GDP above the pre-disaster steady-state level and that disasters destroying mainly productive capital reduce output and GDP. Insignificant responses of output can be expected when disasters destroy both, durable goods and productive capital. In an extension of the model we show that a neutral response of GDP can also be obtained if durable goods and residential structures are destroyed, while physical capital is left intact. The theory explains why the welfare losses entailed by GDP-neutral disasters are substantial and of about the same order of magnitude as those entailed by one-shock-only disasters. As a rule of thumb we estimate that a disaster destroying 20\% of total assets entails a welfare loss of about 3–4\% irrespective of its highly variable and disaster-type specific impact on output and GDP. This result turned out to be very robust against the type of the disaster and the assumed preferences of citizens.

We acknowledge that many countries afflicted by natural disasters receive foreign aid or are (partially) insured against disaster risk. These features can be conceptualized in our model as a transfer to households coming from abroad. This transfer would mitigate the negative wealth effect caused by disasters and hence reduce the positive response of labor supply. We therefore expect that foreign aid or insurance mitigates, but not reverses, the positive channel through which disasters affect output and GDP (Breckner et al. 2016, show that disaster effects on GDP depend on the degree of insurance penetration).

Our study suggests that output and GDP are inferior and misleading indicators of the damage caused by natural disasters. A better proxy would be the lost stock of durable goods, housing and/or productive capital or the discounted aggregate investment expenditure needed to reconstruct the lost stocks.

Our results are insignificantly influenced by the assumed absolute size of the disaster. This fact allowed us to focus the quantitative analysis exemplarily on disasters leading to a loss of 10\% of total assets. For larger or smaller disasters, the estimated welfare loss and—in case of one-shock disasters—the estimated GDP responses vary in proportion with the size of the disaster. Likewise, we can always find a shock composition that implies zero impact of the disaster on GDP, irrespective of the disaster size. This quantitative outcome is a natural consequence of an iso-elastic utility function and an iso-elastic, constant-returns-to-scale production function, the usual ingredients of quantitative macroeconomics.

For very large shocks, however, it seems reasonable to abandon the constant elasticity assumption. In particular, labor supply is likely to be bounded by physiological constraints. The work day is limited by 24 h and for most occupations, physiological limits are reached far earlier. Humans cannot sustain a physical activity level (PAL) of more than 2.4 times the basal metabolic rate for an extended period of time (Westerterp 2001). For example, activities like ‘loading sacks on a truck’ and ‘carrying wood’ are associated with PAL values of 6.6 (FAO 2001), implying that a worker’s energy needs would be 6.6 times his basal metabolic rate if he were occupied with these activities for 24 h. Such a “heavy construction worker” could only manage to exert effort for \( \frac{2.4 \times 24}{6.6} = 8.7 \) h per day. Less energy consuming activities are, of course, sustainable for longer hours. In any case, upper limits to daily labor supply would help to explain why large disasters are more frequently found to exert a negative impact on GDP than small disasters (see Loayza et al. 2012). Extending our model by physiologically-constrained labor supply, for example based on Dalgaard and Strulik (2011), could be a promising task for future research on the macroeconomic implications of natural disasters.
Appendix A

We analyze the phase diagram for subsystem (29) and (30), and show that it has a unique and saddle-point stable steady state. To do this, we show that the $\dot{x} = 0$ isocline and $\dot{d} = 0$ isocline intersect exactly once in the positive quadrant. Saddle-point dynamics can then be inferred from the phase diagram.

The $\dot{d} = 0$ isocline is given by $x = \delta_d d$. Hence, it is linear with positive slope $\delta_d > 0$.

The $\dot{x} = 0$ isocline is given by
\[
(1 + \frac{\psi(x)}{x})(\bar{r} + \delta_d) = \frac{v'(d)}{w'(c)}. \tag{61}
\]
Both isoclines intersect in the positive quadrant. To see this, notice that $\lim_{x \to 0} \psi(x)/x = 0$ and $\lim_{x \to \infty} \psi(x)/x = \infty$ because $\psi$ is strictly convex and $\psi(0) = 0$. Hence, for $d \to 0$, the right-hand side of Eq. (61) converges towards infinity implying that $x \to \infty$, and for $d \to \infty$ the right-hand side of Eq. (61) converges to 0 implying that the $\dot{x} = 0$ isocline intersects the $d$ axis at a finite point. An illustration of both isoclines is shown in Fig. 2.

In order to prove that the intersect of the isoclines is unique, we begin by showing that the slope of the $\dot{x} = 0$ isocline is negative for $x > 0$. By implicit differentiation of (61), we obtain
\[
\frac{dx}{dd} = \frac{\frac{v'(d)}{w'(c)} - \frac{\psi'(x)}{x}}{1 + \frac{\psi(x)}{x}} (\bar{r} + \delta_d) < 0 \quad \forall x > 0. \tag{62}
\]
The numerator is negative, because $v$ is strictly concave, and the denominator is positive, because the strict convexity of $\psi$ together with $\psi(0) = 0$ implies that $\psi'(x) > \psi(x)/x$ for $x > 0$. Together, this implies that the sign of the derivative is negative. Hence, the slopes of the isoclines have opposite signs and the intersection point is unique.

The isoclines divide the phase diagram into four areas. Saddle-point stability follows from the dynamics within these areas: Above the $\dot{d} = 0$ isocline, $\dot{d}$ is positive and below $\dot{d}$ negative; on the right-hand side of the $\dot{x} = 0$ isocline, $\dot{x}$ is positive, and on the left-hand side, $\dot{x}$ is negative.

Appendix B

Here, we present an alternative setup in which households rent housing services from firms. We show that this setup is equivalent to the model in Sect. 2. The alternative setup allows us to derive a rental price for durables, $p_d$.

Households solve
\[
\max_{c, x, h, \ell} \int_0^\infty (u(c) + v(d) + v_h(h) + q(1 - \ell)) \cdot e^{-\rho t} dt, \tag{63}
\]
subject to
\[ \dot{a} = w\ell + ra - c - p_x x - p_h h \] (64)
\[ \dot{d} = x - \delta_d d, \] (65)
where \( p_h \) denotes the price for hiring one unit of residential housing \( h \) for one unit of time. The first order conditions are
\[ u'(c) = \lambda, \] (66)
\[ \lambda p_x = \mu, \] (67)
\[ \lambda h = \lambda p_h, \] (68)
\[ \lambda w = q'(1 - \ell), \] (69)
\[ \lambda r = \lambda \rho - \dot{\lambda}, \] (70)
\[ \dot{\mu} = \mu \rho - v'(d) + \mu \delta_d. \] (71)

We derive an equation for \( p_h \) by combining Eqs. (66) and (68):
\[ p_h = \frac{v'(d)}{u'(c)}. \] (72)

Furthermore, substituting Eq. (66) into (69) yields Eq. (12), and differentiating Eq. (66) with respect to time and combining with Eq. (70) yields the Keynes–Ramsey rule (11). Introducing firms supplying durable investment goods at price \( p_x = 1 + \psi(x)/x \) yields the differential equation for \( x \), Eq. (14).

There exists a continuum \((0, 1)\) of firms buying installed units of houses \( i_h \) from construction firms at price \( p_{i_h} \) and renting houses \( h \) to households. These firms can best be seen as real estate firms whose only role is to buy installed houses and rent them to households. Hence, these firms maximize
\[ \pi = \int_0^\infty (p_h h - p_{i_h} i_h) e^{-rt} dt \] (73)
subject to
\[ \dot{h} = i_h - \delta_h h \] (74)
The first order conditions are
\[ p_{i_h} = \nu, \] (75)
\[ p_h - \nu \delta_h = \nu r - \dot{\nu} \] (76)
with \( \nu \) denoting the shadow price of one installed unit of \( h \) in terms of marginal revenues.

There exists a continuum \((0, 1)\) of construction firms converting final goods into housing. These firms face adjustment costs \( \phi(i_h) \) for installing \( i_h \) units of housing. Each real estate firm is assumed to engage one construction firm per unit of time but it can change the contracting party at any point of time. Free entry into the construction sector implies that firms sell \( i_h \) at unit costs:
\[ p_{i_h} = 1 + \frac{\phi(i_h)}{i_h}. \] (77)
Substituting Eq. (75) into (77), differentiation with respect to time, and substituting (76) and (72) yields
\[ \frac{i_h}{i_h} = \left( \phi'(i_h) - \frac{\phi(i_h)}{i_h} \right)^{-1} \left[ \left( 1 + \frac{\phi(i_h)}{i_h} \right) (r + \delta_h) - \frac{v'(h)}{u'(c)} \right], \] (78)
which is equal to Eq. (53). Hence, the alternative setup for households renting durable goods $h$ from real estate firms is equivalent to the benchmark setup.

**Appendix C**

We show that the steady state of the large economy described by system (33)–(40) is unique, if it exists. We begin by analysing the steady state relationship of investment, capital stock, interest rate and Tobin’s $q$. At the steady state $i = \delta_k k$ holds [from Eq. (33)], and thus capital adjustment costs and marginal capital adjustment costs are both zero, i.e. $\phi(\delta_k k) = \phi'(\delta_k k) = 0$. This means that $q = 1$ [from Eq. (38)], and $r = \partial Af(k, \ell)/\partial k$. Finally, at the steady state $r = \rho$ holds [from Eq. (35)], which pins down the capital-labor ratio.

Second, we exploit the analysis of subsystem (29) and (30) from Sect. 3. From the analysis above we know that a higher steady-state value of $c$ leads to a higher steady state of $x$ and $d$. We can express this insight as a steady-state relationship $x = s(c)$ with $s'(\cdot) > 0$. This means that by substituting for $x$ and rearranging Eq. (39) we obtain

$$k \left( \frac{Af(k, \ell)}{k} - \delta_k \right) = c + s(c) + \psi(s(c)). \quad (79)$$

The equation states a positive relationship between $k$ and $c$ at the steady state.

Next, we show that Eq. (40) constitutes a negative steady-state relation between $k$ and $c$, taking the capital-labor ratio (and thus the marginal product of labor) as given. We do this by evaluating the derivative at the steady state for a constant capital-labor ratio:

$$\left. \frac{dk}{dc} \right|_{(\ell)} = \left. \frac{dk}{dl} \right|_{(\ell)} \cdot \left. \frac{dl}{dc} \right|_{(\ell)} = 1 \cdot \frac{-u''(c)}{q''(1 - \ell)} < 0. \quad (80)$$

The overall derivative is negative because $u''(\cdot) < 0$, $q''(\cdot) < 0$, and $u'(\cdot) > 0$. Equations (79) and (40) both imply a steady-state relationship between $k$ and $c$. Finally, noticing that the slopes of the steady-state Eqs. (40) and (79) are of opposite sign, we conclude uniqueness of the steady state.

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