Assessing the prior event rate ratio method via probabilistic bias analysis on a Bayesian network

Edward W. Thommes1,2 | Salaheddin M. Mahmud3 | Yinong Young-Xu4,5 | Julia Thornton Snider6 | Robertus van Aalst1 | Jason K.H. Lee7,8 | Yuliya Halchenko4 | Ellyn Russo4 | Ayman Chit1,7

1Sanofi Pasteur, Swiftwater, Pennsylvania  
2Department of Mathematics and Statistics, University of Guelph, Guelph, Ontario, Canada  
3Department of Community Health Sciences, College of Medicine, University of Manitoba, Winnipeg, Manitoba, Canada  
4Clinical Epidemiology Program, Veterans Affairs Medical Center, White River Junction, Vermont  
5Department of Psychiatry, Geisel School of Medicine at Dartmouth, Hanover, New Hampshire  
6Precision Health Economics, Oakland, California  
7Leslie Dan School of Pharmacy, University of Toronto, Toronto, Ontario, Canada  
8Sanofi Pasteur, Toronto, Ontario, Canada

Correspondence
Edward W. Thommes, Sanofi Pasteur, Swiftwater, PA 18370; or Department of Mathematics and Statistics, University of Guelph, Guelph, ON N1G 2W1, Canada. Email: edward.thommes@sanofi.com

**Background:** Unmeasured confounders are commonplace in observational studies conducted using real-world data. Prior event rate ratio (PERR) adjustment is a technique shown to perform well in addressing such confounding. However, it has been demonstrated that, in some circumstances, the PERR method actually increases rather than decreases bias. In this work, we seek to better understand the robustness of PERR adjustment.

**Methods:** We begin with a Bayesian network representation of a generalized observational study, which is subject to unmeasured confounding. Previous work evaluating PERR performance used Monte Carlo simulation to calculate joint probabilities of interest within the study population. Here, we instead use a Bayesian networks framework.

**Results:** Using this streamlined analytic approach, we are able to conduct probabilistic bias analysis (PBA) using large numbers of combinations of parameters and thus obtain a comprehensive picture of PERR performance. We apply our methodology to a recent study that used the PERR in evaluating elderly-specific high-dose (HD) influenza vaccine in the US Veterans Affairs population. That study obtained an HD relative effectiveness of 25% (95% CI: 2%-43%) against influenza- and pneumonia-associated hospitalization, relative to standard-dose influenza vaccine. In this instance, we find that the PERR-adjusted result is more like to underestimate rather than to overestimate the relative effectiveness of the intervention.

**Conclusions:** Although the PERR is a powerful tool for mitigating the effects of unmeasured confounders, it is not infallible. Here, we develop some general guidance for when a PERR approach is appropriate and when PBA is a safer option.

**KEYWORDS**
Bayesian networks, observational studies, probabilistic bias analysis, prior event rate ratio (PERR), unmeasured confounders

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INTRODUCTION

From healthcare to econometrics to the social sciences, the findings of observational studies almost always suffer from bias due to confounding. Numerous methods to control for confounding have been developed, and for each of these, dealing with unmeasured confounders usually presents the trickiest challenge.

One method that has been used to address confounding due to unmeasured variables is prior event rate ratio (PERR) adjustment, developed by Weiner and colleagues and shown to perform well in reproducing the results of a Scandinavian randomized controlled trial (RCT) with an observational study conducted using UK Electronic Medical Record (EMR) data. Subsequent work by Weiner et al showed a similarly good performance of PERR applied to observational studies in replicating other RCTs. Uddin et al studied the performance of PERR and identified situations in which PERR adjustment increases rather than decreases bias. Further development and refinement, including derivation from PERR adjustment of a pairwise Cox likelihood function, was carried out by Lin and Henley.

Here, we endeavor to understand when PERR yields meaningful bounds on the size and/or direction of the treatment effect of interest, even if it cannot be guaranteed to remove (or even reduce) bias. We begin with a Bayesian network representation of the causal pathways in a standard observational study (Figure 1). We use Bayesian network analysis to define exact analytic expressions for the joint probabilities of study variables. (Uddin et al used Monte Carlo simulation to approximate the joint probabilities.) We examine the behavior of the system and identify circumstances where the PERR method overestimates and underestimates the true effect of a treatment. As an illustrative example, we then apply our approach to performing a probabilistic bias analysis (PBA) of a study of the relative effectiveness of high-dose (HD) versus standard-dose (SD) seasonal influenza vaccine in the Veterans Affairs (VA) patient population.

THE PERR METHOD

Let us suppose we are conducting a cohort study in which the rate of the outcome of interest is measured not just during the observation period after the treatment but also during a baseline period before the treatment. We denote a possible event occurring during the baseline period as \( Y_1 \), a possible event occurring during the observation period as \( Y_2 \) and a possible treatment as \( X \). The variables are dichotomous, so, for example, an individual with \( (Y_1 = y_1, X = \bar{x}, Y_2 = \bar{y}_2) \) experienced an event in the baseline period, did not receive the treatment and did not experience an event in the observation period. To streamline the notation, we will write \( Y_1 = y_1 \) as \( y_1 \), etc. We use \( P \) to denote the probability, over a time interval \( T \), that an event occurs in an individual. For example, \( P(y_2 | x) \) is the probability per time \( T \) that an individual experiences an event in the observation period, conditional on having received treatment. Measured at the population level, \( P \) becomes the average incidence rate, ie, events per person per time \( T \). We denote the incidence rate as \( R \). Since the two quantities are numerically identical (assuming that both are defined over the same unit of time, and that individuals are independent), we will use them interchangeably. The incidence rate ratio (RR) in the baseline period is then

\[
RR_{\text{base}} = \frac{R(y_1 | x)}{R(y_1 | \bar{x})},
\]

whereas, in the observation period, it is

\[
RR_{\text{obs}} = \frac{R(y_2 | x)}{R(y_2 | \bar{x})}.
\]

Now, let us suppose that we find \( RR_{\text{base}} \) for the event to differ from unity by a statistically significant amount. This suggests that the treatment and control arms are unbalanced with respect to the distribution of one or more determinants of the event. Assuming that there are no systematic measurement errors and that all measurable confounders have already been

FIGURE 1 Bayesian network, or probabilistic directed acyclic graph, with dichotomous variables denoting baseline period event \( Y_1 \), treatment \( X \), observation-period event \( Y_2 \), time-varying unobserved confounder \( [C_{1a}, C_{1b}, C_2] \), and the rate ratios (RRs) describing the associations among them. The RRs are defined in Equations (10) to (18) [Colour figure can be viewed at wileyonlinelibrary.com]
controlled for, we are led to suspect that there is residual unmeasured confounding by indication. The PERR method attempts to correct for the imbalance and thus recover the “true” RR of the treatment through normalizing \( \text{RR}_{\text{obs}} \) by \( \text{RR}_{\text{base}} \)

\[ PERR = \frac{\text{RR}_{\text{obs}}}{\text{RR}_{\text{base}}} \]  

(3)

3 | THE CAUSAL MODEL

We begin with a Bayesian network (or probabilistic directed acyclic graph [DAG])\(^7\) depicting, from the perspective of a single individual, the potential causal associations in our study. We include an unmeasured dichotomous confounder, \( C \in \{c, \bar{c}\} \). We define distinct values for the confounder in the baseline period (\( C_1 \)) and the observation period (\( C_2 \)). We further divide \( C_1 \) into \( C_{1a} \) and \( C_{1b} \) to allow for the possibility that the relationship between \( C_1 \) and \( Y_1 \) is bidirectional (ie, the state of \( C_1 \) influences the state of \( Y_1 \), and the state of \( Y_1 \) influences the state of \( C_1 \)). We also allow for the possibility of a direct causal connection between baseline event \( Y_1 \) and treatment \( X \). One can show (see the work of Greenland et al\(^7\)) that this DAG has a null adjustment set and that there exist no instruments or conditional instruments that might permit instrumental variable regression.

We write down a set of equations that describe this causal diagram. The effect of each directed edge is expressed as an RR whose value depends on the state of the variable corresponding to the edge’s originating vertex. The model equations describing the population-level incidence rates \( R \) (or equivalently, individual-level probabilities \( P \)) over a time period \( T \) of the occurrence of \( c, y_1, x, \) and \( y_2 \) are

\[ R(C_{1a} = c_{1a}) = P(C_{1a} = c_{1a}) = r_{c1a} \]  

(4)

\[ R(Y_1 = y_1|C_{1a}) = P(Y_1 = y_1|C_{1a}) = \Pi_{[0,1]}(r_{y1} \cdot \text{RR}_{C_{1a} \rightarrow Y_1}) \]  

(5)

\[ R(C_{1b} = c_{1b}|C_{1a}, Y_1) = P(C_{1b} = c_{1b}|C_{1a}, Y_1) = \Pi_{[0,1]}(r_{c1b} \text{RR}_{Y_1 \rightarrow C_{1b}} \text{RR}_{C_{1a} \rightarrow C_{1b}}) \]  

(6)

\[ R(X = x|C_{1b}, Y_1) = P(X = x|C_{1b}, Y_1) = \Pi_{[0,1]}(r_{x} \cdot \text{RR}_{C_{1b} \rightarrow X} \cdot \text{RR}_{Y_1 \rightarrow X}) \]  

(7)

\[ R(C_2 = c_2|C_{1b}) = P(C_2 = c_2|C_{1b}) = \Pi_{[0,1]}(r_{c2} \cdot \text{RR}_{C_{1b} \rightarrow C_2}) \]  

(8)

\[ R(Y_2 = y_2|C_2, Y_1, X) = P(Y_2 = y_2|C_2, Y_1, X) = \Pi_{[0,1]}(r_{y2} \cdot \text{RR}_{C_2 \rightarrow Y_2} \cdot \text{RR}_{Y_1 \rightarrow Y_2} \cdot \text{RR}_{X \rightarrow Y_2}) \]  

(9)

where \( r_{c1a}, r_{y1}, r_{c1b}, r_{x}, r_{c2}, r_{y2} \) are constants on \([0,1]\). The operator \( \Pi_{[0,1]}(x) \in \mathbb{R} \), is the closest-element mapping from real numbers to \([0,1] \), ie,

\[ \Pi_{[0,1]}(x) = \begin{cases} 
0, & \text{if } x < 0 \\
 x, & \text{if } x \in [0, 1] \\
1, & \text{if } x > 1.
\end{cases} \]

(10)

The RRs are defined as follows:

\[ \text{RR}_{C_{1a} \rightarrow Y_1} = \begin{cases} 
F_{c1a \rightarrow Y_1}, & \text{if } C_{1a} = c_{1a} \\
1, & \text{if } C_{1a} = \overline{c_{1a}}
\end{cases} \]  

(11)

\[ \text{RR}_{Y_1 \rightarrow C_{1b}} = \begin{cases} 
F_{Y_1 \rightarrow C_{1b}}, & \text{if } Y_1 = y_1 \\
1, & \text{if } Y_1 = \overline{y_1}
\end{cases} \]  

(12)

\[ \text{RR}_{C_{1a} \rightarrow C_{1b}} = \begin{cases} 
F_{c1a \rightarrow C_{1b}}, & \text{if } C_{1a} = c_{1a} \\
1, & \text{if } C_{1a} = \overline{c_{1a}}
\end{cases} \]  

(13)

\[ \text{RR}_{C_{1b} \rightarrow X} = \begin{cases} 
F_{c1b \rightarrow X}, & \text{if } C_{1b} = c_{1b} \\
1, & \text{if } C_{1b} = \overline{c_{1b}}
\end{cases} \]  

(14)

\[ \text{RR}_{Y_1 \rightarrow X} = \begin{cases} 
F_{y1 \rightarrow X}, & \text{if } Y_1 = y_1 \\
1, & \text{if } Y_1 = \overline{y_1}
\end{cases} \]  

(15)
where the F's are constants >0.

Uddin et al used Monte Carlo simulation to obtain approximate conditional rates/probabilities from this model. Instead, we will use Bayesian network analysis (see, eg, the work of Pearl) to calculate exact probabilities, as follows.

The incidence rate with which a given set of values of $C_{1a}, Y_1, C_{1b}, X, C_2,$ and $Y_2$ is realized on the above network is their joint probability

$$R(C_{1a}, Y_1, C_{1b}, X, C_2, Y_2) = P(C_{1a}, Y_1, C_{1b}, X, C_2, Y_2) = P(C_{1a}) P(Y_1|C_{1a}) P(C_{1b}|C_{1a}|Y_1) P(X|C_{1a}, Y_1, C_{1b}) P(C_2|C_{1a}|Y_1|C_{1b}|X) P(Y_2|C_{1a}, Y_1, C_{1b}, X, C_2).$$

Joint rates/probabilities of subsets of the variables are calculated by summing the joint probabilities over all possible combinations of the remaining variables, for example,

$$R(y_1, x) = P(y_1, x) = \sum_{\{c_{1a}\}} \sum_{\{c_{1b}\}} \sum_{\{c_2\}} \sum_{\{y_2\}} P(C_{1a}, Y_1 = y_1, C_{1b}, X = x, C_2, Y_2).$$

Conditional rates/probabilities can likewise be calculated, for example,

$$R(y_1|x) = P(y_1|x) = \frac{P(y_1, x)}{P(x)},$$

where

$$R(x) = P(x) = \sum_{\{c_{1a}\}} \sum_{\{c_{1b}\}} \sum_{\{c_2\}} \sum_{\{y_2\}} P(C_{1a}, Y_1, C_{1b}, X = x, C_2, Y_2).$$

We implement these calculations in the R language.

### 4 THE PERFORMANCE OF PERR ADJUSTMENT

In an observational study, the following incidence rates will be measured:

- $R(x)$, the rate of treatment across the study population;
- $R(y_2|x)$, the rate of the event in the treatment arm during the observation period;
- $R(y_2|x)$, the rate of the event in the control arm during the observation period;
- $R(y_2)$, the rate of the event across the whole study population during the observation period (where $R(y_2) = R(y_2|x)R(x) + R(y_2|x)R(\overline{x})$).

If patients have also been observed during a baseline period, then we further have measurements of the following:

- $R(y_1|x)$, the rate of the event in the treatment arm during the baseline period (ie, the rate among those who are later treated);
- $R(y_1|x)$, the rate of the event in the control arm during the baseline period (ie, the rate among those who are not later treated);
- $R(y_1)$, the rate of the event across the whole study population during the baseline period (where $R(y_1) = R(y_1|x)R(x) + R(y_1|x)R(\overline{x})$).
The RRs between treatment and control arms in the observation and baseline period are given by Equations (1) and (2), respectively, while the PERR estimate of the treatment effect is given by Equation (3).

The true, unbiased effect of treatment \( x \) on the probability of event \( y_2 \) is given by \( F_x \rightarrow y_2 \) (see Equation (18)). The question we wish to answer for our causal model is, under what circumstances does PERR succeed in decreasing bias, and under what circumstances does it actually increase bias? Furthermore, under what circumstances is the \( PERR \) estimate either \(<F_x \rightarrow y_2 \) or \( >F_x \rightarrow y_2 \)? For specificity, we take events \( y \) to be harmful, thus the smaller \( F_x \rightarrow y_2 \), the more effective the treatment \( x \). Therefore, when \( PERR/F_x \rightarrow y_2 < 1 \), the effectiveness of \( x \) is overestimated (overoptimistic PERR), whereas if \( PERR/F_x \rightarrow y_2 > 1 \), it is underestimated (pessimistic PERR).

We begin by computing the behavior of the PERR in comparison to the true effect \( F_x \rightarrow y_2 \) under different scenarios.

1. Unobserved confounder effect is present and affects the baseline and observation period event probability equally (ie, \( F_{c2} \rightarrow y_2 = F_{cia} \rightarrow y_1 \neq 1 \)) and also affects the probability of treatment (ie, \( F_{clb} \rightarrow x \neq 1 \)), while \( F_{y1} \rightarrow x \) is fixed at 1. Baseline period events do not affect the probability that the confounder is present (ie, \( F_{y1} \rightarrow clb = 1 \)). Figure 2 shows \( RR_{obs} \), the PERR, and the true effect \( F_x \rightarrow y_2 \) as a function of \( F_{cia} \rightarrow y_1 \). As we can see, even though \( RR_{obs} \) diverges from the true effect, the PERR is exactly equal to the true effect.

2. Retaining the effect of the unobserved confounder, we allow \( F_{y1} \rightarrow y_2 \), the effect of the occurrence of a baseline event on the likelihood of an observation period event, to vary. Results are shown in Figure 3. As can be seen, increasing \( F_{y1} \rightarrow y_2 \) above 1 makes the PERR progressively more pessimistic (ie, \( PERR/F_x \rightarrow y_2 \) increases above 1), though the effect is relatively weak and bounded.

3. We allow \( F_{c2} \rightarrow y_2 \) to differ from \( F_{cia} \rightarrow y_1 \). Results are shown in Figure 4. When \( F_{cia} \rightarrow y_1 < F_{c2} \rightarrow y_2 \), (ie, the effect of the confounder on likelihood of an event is weaker in the baseline period than in the observation period), the PERR is pessimistic; when the converse is true, \( F_{cia} \rightarrow y_1 > F_{c2} \rightarrow y_2 \), then the PERR is overoptimistic. As we will see later

**FIGURE 2** The conventional rate ratio (RR) \( (RR_{obs}) \), the prior event rate ratio (PERR) estimator, and the true RR \( (RR_x \rightarrow y_2 \) set to 0.7) in the case where \( C_{ia} = C_{ib} = C_1 \) and \( F_{cia} \rightarrow y_1 = F_{cia} \rightarrow y_1 \). \( F_{clb} \rightarrow x \) is held fixed at 1.5, and \( r_{cia} = 0.25 \). Note that the PERR and the true RR are coincident.

**FIGURE 3** Performance of the prior event rate ratio (PERR) estimator as a function of \( F_{y1} \rightarrow y_2 \). The ratio of the PERR to the true effect, ie, \( F_x \rightarrow y_2 \), is plotted. A ratio greater than 1 thus corresponds to an overestimate of the true RR and, hence, an underestimate of the true treatment effect. Scenarios with \( F_{cia} \rightarrow y_1 = 1 \) (Scenario a), \( 2 \) (Scenario b), \( 3 \) (Scenario), and \( 4 \) (Scenario d) are shown. As before, we set \( C_{ia} = C_{ib} = C_2 \), \( F_{cia} \rightarrow y_2 = F_{cia} \rightarrow y_1 \), and fix \( F_{clb} \rightarrow x = 1.5 \), \( r_{cia} = 0.25 \). In each case, the overestimate of the true rate ratio (RR) by the PERR initially becomes greater with \( F_{y1} \rightarrow y_2 \), then reaches a maximum, and decreases again. The height of the maximum increases with \( F_{cia} \rightarrow y_1 \). When \( F_{cia} \rightarrow y_1 = 4 \), the maximum PERR overestimate of the true RR is 15% and occurs when \( F_{y1} \rightarrow y_2 = 4 \).
Accuracy of the prior event rate ratio (PERR) estimator as a function of $F_{c1 \rightarrow X}$, with $F_{c1 \rightarrow Y_1}$ held fixed at 3. In Scenario a, $F_{c1 \rightarrow X} = 1.5$, whereas in Scenario b, $F_{c1 \rightarrow X} = 1.9$. As before, $r_{c1a} = 0.25$.

Performance of the prior event rate ratio (PERR) estimator when $F_{y_1 \rightarrow X}$ differs from 1. In Scenario a, there are no confounders, i.e., $r_{c1a} = 0$, and as before, $C_2 = C_{1b} = C_{1a}$. In Scenario b, the confounder is present ($r_{c1a} = 0.25$), with $F_{c2 \rightarrow Y_2} = F_{c1a \rightarrow Y_1} = 3$ and $F_{c1b \rightarrow X} = 1.5$.

(Section 5 and Appendix A), one reason that these two values may differ is if the effect of treatment $x$ in an individual changes depending on whether the confounder is present or absent.

4. We allow $F_{y_1 \rightarrow X}$ to differ from 1; see Figure 5. Above 1, even modest values of $F_{y_1 \rightarrow X}$ suffice to make the PERR substantially overoptimistic. Conversely, as $F_{y_1 \rightarrow X}$ is decreased below 1, PERR rapidly becomes more pessimistic. Note that $F_{y_1 \rightarrow X}$ cannot exceed $r_{X1}^{-1}$, otherwise $P(X = x)$ would exceed 1 for individuals having a baseline event $y_1$.

5. We reverse the directionality of the baseline period relationship between confounder and event: while a pre-existing confounder $c_1$ does not affect the probability of a baseline event $y_1$, an individual without pre-existing $c_1$ may develop $c_1$ as a result of experiencing $y_1$. Figure 6 shows that, as the strength of the association $F_{y_1 \rightarrow C_{1b}}$ increases, PERR becomes increasingly overoptimistic. Depending on the pre-existing confounder incidence rate $r_{c1a}$, and on $F_{c1b \rightarrow X}$, $PERR/F_{x \rightarrow Y_2}$ may or may not have a lower limit $>0$.

6. We allow for the possibility that an individual either loses or gains the confounder between baseline and observation period. We see from Figure 7 that both scenarios act to make PERR overoptimistic; by how much depends on $F_{c1a \rightarrow Y_1}$ and $F_{c1b \rightarrow X}$.

We thus see that the PERR works just as intended as long as the association between confounder and events has the same strength in the baseline and observation periods. The more confounding differs between the periods, though, the poorer the PERR does as an estimator of the true effect. Whether the strength of confounding increases or decreases with time is important, because this determines whether the PERR overestimates or underestimates, respectively, the true effect of the intervention.

We also see that the PERR is overoptimistic when there is a causal connection directed from baseline period event $y_1$ to treatment $x$, either directly or via confounder $C_{1b}$. Finally, PERR is overoptimistic when individuals are able to either gain or lose the confounder over the course of the study period.
FIGURE 6  Performance of the prior event rate ratio (PERR) estimator when the directionality of the causal relationship between baseline confounder and $Y_1$ is reversed, i.e., $F_{c_{1a}} \rightarrow Y_1 = 1$ (presence of $c_{1a}$ does not affect probability that $Y_1$ is present), $F_{y_{1} \rightarrow C_{1b}} > 1$ (presence of $Y_1$ increases the probability that $c_{1b}$ is present), and as above, $c_{1b} = c_{1a}$. Scenario a: $r_{c_{1a}} = 0.25$. Scenario b: $r_{c_{1a}} = 0.5$. Scenario c: $r_{c_{1a}} = 0.25$, $F_{c_{1a} \rightarrow X}$ is increased from 1.5 to 3.

FIGURE 7  Performance of the prior event rate ratio (PERR) estimator when the value of $C_2$ is allowed to differ from the value of $C_{1b}$ (in all cases $C_{1b} = C_{1a}$). Scenario a: $r_{c_2} = r_{c_{1a}} = 0.25$ and $F_{c_{1b} \rightarrow X}$ increased from 1.5 to 3. Scenario b: As in Scenario a but with $F_{c_{1b} \rightarrow X}$ increased from 1.5 to 3. Scenario c: $P(c_2|c_{1b}) = 0.5$, $P(c_2|c_{1b}) = 0$ (ie, probability of losing confounder is 0.5).

4.1  Probabilistic bias analysis

We have investigated ways in which using the PERR to control for unobserved confounding can fail. However, if one has sufficient information to be able to place limits on the strengths of the causal associations among the study subjects’ set of attributes \{C_{1a}, Y_1, C_{1b}, X, C_2, Y_2\}, and the incidence rates of the unobserved confounders, one may still be able to obtain useful constraints on the true treatment effect via PBA.\textsuperscript{11}

The approach is straightforward: one chooses prior probability distributions for the incidence rates of the unobserved confounder, and for each of the factors $F$ governing the associations among the attributes, except for the treatment effect itself, $F_x \rightarrow Y_2$. One then performs iterations of drawing a set of values from these distributions. For each set, one computes the value of $F_x \rightarrow Y_2$ needed to realize the observed rates $R(X)$, $R(Y_1|X)$, $R(Y_1|\overline{X})$, $R(Y_2|X)$, and $R(Y_2|\overline{X})$. In this way, one obtains a posterior distribution of possible values of the true treatment effect. The number of iterations should be sufficiently large that increasing it further does not appreciably change the shape of the posterior distribution. Here, we implement all of the above in R and perform 50 000 iterations for each scenario.

5  APPLICATION TO AN OBSERVATIONAL STUDY

We apply our method to a study of HD influenza vaccine effectiveness, relative to SD vaccine, against influenza and influenza-associated outcomes that was conducted within the VA patient population by Young-Xu et al.\textsuperscript{9} In this study, a difference in the rate of hospitalization for pneumonia and influenza (P&I; ICD-9 codes 480-488) in the HD and SD arms was found in the baseline period even after matching on patient comorbidities, suggesting residual confounding by
indication. This was addressed through use of PERR adjustment. We will apply the above PBA methodology to assess the robustness of this approach in this particular study.

For the baseline period, the study reported event rates (in units of events per 10 000 person-weeks) of $R_{HD,\text{base}} = 3.24$ and $R_{SD,\text{base}} = 2.1$. For the observation period, the rates were $R_{HD,\text{obs}} = 3.45$, $R_{SD,\text{obs}} = 2.98$. Thus, the RRs of HD versus SD arms in the baseline and observation periods were $RR_{base} = 1.54$ and $RR_{obs} = 1.16$, respectively. This made the unadjusted relative effectiveness $rVE_{HD,\text{obs}} = 1 - RR_{obs} = -16\%$, suggesting (contrary to evidence from its RCT12) that the HD vaccine was less effective than SD. However, the fact that the RR in the baseline period differed significantly from 1 ($RR_{base} = 1.54$) suggested confounding by indication. The PERR estimate of the RR was

$$RR_{PERR} = \frac{RR_{obs}}{RR_{base}} = 0.75,$$

for an HD to SD relative effectiveness

$$rVE_{HD,PERR} = 100\% \cdot (1 - RR_{perr}) = 25\% \cdot 23\%,$$

where the confidence interval was obtained using the assumption of Poisson-distributed events. We apply the causal diagram of Figure 1 to this study, with the following interpretation: starting in the baseline period, an unobserved confounder $C$ that is present in part of the patient population—we can think of it as frailty not captured in the patients’ medical records—potentially causes one or more of the following:

1. an elevated likelihood of hospitalization for pneumonia/influenza during the baseline period;
2. a modified likelihood of receiving HD rather than SD vaccine via confounding by indication: the presence of $C_1$ increases the likelihood that the healthcare provider (HCP) will identify the patient as being at elevated risk, and this may then affect the HCP’s decision whether to prescribe SD or HD;
3. an elevated likelihood that the patient will also possess the confounder in the observation period, ie, $C_2 = c_2$ (a frail patient is likely to remain frail);
4. if the confounder does carry over into the observation period, then an elevated likelihood of hospitalization for pneumonia/influenza during the observation period; and
5. a reduced immune response to vaccination, resulting in a reduction in the protective effect derived from both HD and SD.

Point 5 requires further explanation. It has been shown that frailty can substantially reduce the effectiveness of influenza vaccine against influenza-associated hospitalization.13 Furthermore, it has been shown that the relative efficacy of HD versus SD does not vary significantly between frail and nonfrail individuals.14 We thus make the assumption that frail individuals receive a weakened vaccine effect, such that the RR due to vaccination is multiplied by a factor $f > 1$ for both HD and SD vaccination. It can be shown (see Appendix A) that this is equivalent to increasing $F_{c_2 \rightarrow y_2}$ by the same factor, which, in turn, suggests that $F_{c_2 \rightarrow y_2} > F_{c_2 \rightarrow y_2}$. In our PBA in the following (and in some of the additional analyses in Appendix B), we use the parameterization $F_{c \rightarrow y_2} = fF_{c \rightarrow y_1}$. From Section 4, we know that, when $f \geq 1$, this puts us in the regime of a pessimistic PERR, ie, one that will underestimate the relative effectiveness of HD, all other things being equal.

In the context of this study, the edge directed from $Y_1$ to $X$ in Figure 1 represents the possibility that the HCP’s choice of vaccine is directly influenced by whether or not a patient was hospitalized for pneumonia/influenza during the baseline period. P&I hospitalization can also influence vaccine choice by the causal path from $Y_1$ to $C_{1b}$ to $X$: hospitalization may cause frailty (instead of/in addition to the other way around), and the presence of this newly acquired frailty may then influence vaccine choice. As we saw in Section 4, both the direct and indirect path can cause the PERR to be overoptimistic.

To investigate the possibility of a direct link from $Y_1$ to $X$, we conducted an interview study among nurse infection preventionists in 25 Veterans Health Administration (VHA) facilities to gain understanding of the decision-making process governing the selection of HD versus SD for a given patient within VA facilities. The study is described in Appendix C. In no case was previous hospitalization for pneumonia/influenza reported as a criterion for preferentially administering HD. On the contrary, in two (8%) of the facilities, recent hospitalization for pneumonia was reported as a possible contra-indication for HD administration. This suggests that $F_{y_1 \rightarrow X} \leq 1$. 

\[ RR_{PERR} = \frac{RR_{obs}}{RR_{base}} = 0.75, \]

\[ rVE_{HD,PERR} = 100\% \cdot (1 - RR_{perr}) = 25\% \cdot 23\%. \]
We conduct our probabilistic bias analyses by performing Monte Carlo simulations consisting of 50,000 realizations each (some of these are discarded due to having infeasible combinations of inputs). Each realization proceeds via a “draw and adjust” procedure, as follows.

1) A set of observed values for $R(y_1|x), R(y_1|x), R(y_2|x)$, and $R(y_1|x)$ is drawn from the results of the study of Young-Xu et al, assuming, as they do, that event counts are Poisson-distributed.
2) All DAG parameters apart from $F_{1b} \rightarrow x, r_x, F_x \rightarrow y_2$ and $r_y$ are drawn from their respective prior distributions, and any required relationships among parameters are imposed.
3) $F_{1b} \rightarrow x$ is chosen such that $R(y_1|x)$ is reproduced.
4) $r_x$ is chosen such that $R(x)$, the study HD vaccination rate, is reproduced.
5) $F_x \rightarrow y_2$ is chosen such that $RR_{obs} = \frac{R(y_2|x)}{R(y_2|x)}$ is reproduced.

The output of each realization is the posterior distribution of $F_x \rightarrow y_2$, the true treatment effect, where $r_{VE_{HD,true}} = 100 \% \cdot (1 - F_x \rightarrow y_2)$.

We choose uniform distributions for all input parameters. In Appendix B, we examine the effect of applying progressively more constraints on the input parameter ranges and relationships among them (Table B1). Corresponding posterior distributions of $r_{VE_{HD,true}}$ are shown in Figure B1. As can be seen, under minimal assumptions (Analysis 1), PERR is very likely to significantly overestimate $r_{VE_{HD}}$. The distribution of $r_{VE_{HD,true}}$ becomes tighter and/or moves further to the right in each successive analysis, and for Analyses 6 and 7, PERR is more likely to underestimate than overestimate the true effect size.

We now seek to identify specific constraints appropriate for this study. Table 1 gives a set of constraints, informed by published literature, on the relationship between hospitalization and frailty state transitions (see the work of Gill et al\textsuperscript{15}) and on hospitalization rates, including for P&I, of high-risk and low-risk individuals (see the work of Mullooly et al\textsuperscript{16}). In using the latter, we assume that the RR of P&I hospitalization of high-risk versus low-risk subjects can be used as a proxy for that of frail versus nonfrail subjects. The results of the PBA are given in Table 2, shown graphically in Figure 8, and compared to the PERR estimate in the study of Young-Xu et al.\textsuperscript{9} Both distributions have a similar lower 95% CI bound, but both the median and upper bound of the PBA posterior distribution are higher than those of the PERR estimate. In Table 1, we compare the distributions using two different metrics: the common-language effect size (CLES)\textsuperscript{17} and the two-sample Hodges-Lehmann estimator\textsuperscript{18} for the difference between two populations. The CLES gives the probability that a sample drawn from the distribution of $r_{VE_{HD,PERR}}$ is greater than a sample drawn from the distribution of $r_{VE_{HD,true}}$. In other words, it gives the probability that PERR overestimates the true effect size. The two-sample Hodges-Lehmann estimator is a nonparametric estimator of the median difference between a pair of samples drawn from the two distributions. Both comparisons suggest that the PERR estimate in the study of Young-Xu et al is more likely to have underestimated than overestimated the true relative effectiveness of HD vaccine.

6 | DISCUSSION

In multiple studies,\textsuperscript{1-3} PERR adjustment has been demonstrated to perform well in controlling for bias due to unmeasured confounding. The method is also appealing due to its relative simplicity, both conceptually and in implementation.
## TABLE 1  
Input parameter ranges for probabilistic bias analysis (PBA) of the study of Young-Xu et al, together with literature sources/rationales

| PBA input parameters                                                                 | Constraints | Source                                | Comments                                                                                                                                                                                                 |
|-------------------------------------------------------------------------------------|-------------|---------------------------------------|----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| RR of direct effect of baseline hospitalization on probability of HD receipt ($F_{y_1 \rightarrow X}$) | [0.9, 1.1]  | Veterans Health Administration Survey study, Appendix C | 6-month incidence rate of transition from nonfrail to frail state (their Table 1)                                                                                                                        |
| Probability that nonfrail subject becomes frail within baseline period ($r_{0tb}$)   | [0.011, 0.024] | 15                                    | 6-month incidence rate of transition from nonfrail to frail state (their Table 1)                                                                                                                        |
| Probability that subject frail in baseline period becomes nonfrail in observation period ($P(C_2 | C_1 b)$) | [0.0006, 0.0036] | 15                                    | $f > 1$ follows from assumption that frail individuals derive less protection from vaccine than nonfrail                                                                                               |
| Relationship between frailty effect on hospitalization in observation and baseline period: ($f \equiv \frac{P(C_2 | C_1 b)}{P(C_1 b)}$) | [1, 10]     | Appendix A13,14                       | Hazard ratio of transition rate from frail to nonfrail state after hospitalization, vs. no intervening hospitalization (their Table 2)                                                              |
| RR of effect of baseline hospitalization on baseline frailty: ($F_{y_1 \rightarrow C_1 b}$) | [1.06; 1.66] | 15                                    | 6-month incidence rate of transition from nonfrail to frail state (their Table 1)                                                                                                                        |
| Probability that subject nonfrail in baseline period becomes frail in observation period ($r_{23}$) | [0.011; 0.024] | 15                                    |                                                                                                                                                                                                          |
TABLE 2   Output of the probabilistic bias analysis (inputs described in Table 1): posterior distribution of the true treatment effect, and comparison to the prior event rate ratio (PERR) estimate in the study of Young-Xu et al.9

| $rVE_{HD,true}(\%)$ | Comparison to $rVE_{HD,PERR} = 25(2:42)\%$ |
|---------------------|------------------------------------------|
| Common-language effect size: Two-sample Hodges-Lehmann probability that PERR overestimates true effect, ie, $P(rVE_{HD,PERR} > rVE_{HD,true})$ | estimate of median difference (%) (a positive value is a PERR overestimate) |
| 34 (0; 42) | 0.28 | −11 |

However, it has been shown that this method may in some cases increase rather than decrease bias.5 We further explored PERR performance and used Bayesian network calculations applied to the causal diagram representation of a previously published observational study of the relative effectiveness of HD versus SD influenza vaccine in the US VA patient population. Using PBA, we showed that, in applying the PERR estimator to control for unmeasured confounding, this particular study is more likely to have underestimated rather than overestimated the true effect size.

This is not to argue that the PERR should be categorically discarded in favor of PBA on Bayesian networks. Under appropriate conditions, the PERR alone will suffice. With reference to the causal diagram of Figure 1, the PERR can safely be used if all of the following apply:

(i) A direct causal association between baseline period event $Y_1$ and treatment $X$ can be ruled out. Such an association can masquerade as an unmeasured confounder, and naïve application of the PERR in this case acts to increase rather than decrease bias.

(ii) There is no variation in the strength of the confounder effect between baseline and observation period.

(iii) Individuals can neither gain nor lose the confounder during the study period.

(iv) A bidirectional relationship between confounder and baseline-period event can be ruled out; that is, presence of a baseline event does not affect the probability that the confounder is present.

(v) No direct causal association between baseline period event $Y_1$ and observation period event $Y_2$ exists. In practice, this is the least critical constraint, since the effect of such an association on the accuracy of the PERR estimator is modest and bounded.

If (i) or (ii) is violated, but one knows the directionality of the relationship, then, depending on the study question, the PERR may still be able to provide a useful constraint on the treatment effect.

This work is subject to a number of limitations. To begin with, although the causal diagram we use is relatively generic, it by no means constitutes an adequate description of every possible type of real-world study. For example, loss of study subjects due to mortality or dropout is not taken into account. In our example of the study of Young-Xu et al.,9 no subjects were lost during the baseline period, and less than 3% were lost during the observation period (unpublished data). Uddin et al.5 did consider loss of subjects and showed that this will cause the PERR to overestimate the treatment effect. For a loss rate of less than 5%, they showed underestimation by well below 1%. However, any study in which mortality/dropout plays a more significant role will need to add this effect into the model. Also, because PERR involves repeat measurements of the same population, correlation effects may be present. In the study of Young-Xu et al, this issue, as well as the possibility of cluster effects at the VA facility level, was addressed by conducting a sensitivity analysis using generalized estimating equations. Even so, our analysis abstracts time dependence into simply a baseline and an observation period. Studies in which time evolution of subjects is more complex will need to utilize a correspondingly more complex DAG, for example, one in which baseline and observation are broken down into multiple subperiods. It should also be emphasized that, in our PBA re-analysis of the study of Young-Xu et al, the sources we use to constrain PBA inputs are derived from a targeted literature search, not an exhaustive literature review. More broadly, any analysis of this type can only be as valid as the DAG that informs it. The construction of a DAG ultimately relies on expert opinion, and no amount of expert opinion can guarantee that a causal link will not be misspecified or overlooked.

Despite the above limitations, our study offers an approach to understanding under what scenarios the PERR is likely to provide an unbiased estimate of the treatment, and a methodology to bound the bias when it is present.
DISCLOSURES

E. Thommes, R. van Aalst, J. Lee, and A. Chit are employees of Sanofi Pasteur. S. Mahmud and Y. Young-Xu have received funding from Sanofi Pasteur in the context of this and previous studies. J. Snider is an employee of and holds equity in Precision Health Economics, which has received consulting fees from Sanofi Pasteur for this and previous studies.

DATA AVAILABILITY STATEMENT

The computer code used to generate the results of this study is included in the published article’s supplementary information files.

ORCID

Edward W. Thommes https://orcid.org/0000-0001-6800-2000

REFERENCES

1. Weiner MG, Xie D, Tannen RL. Replication of the Scandinavian simvastatin survival study using a primary care medical record database prompted exploration of a new method to address unmeasured confounding. Pharmacoepidemiol Drug Saf. 2008;17(7):661-670.
2. Tannen RL, Weiner MG, Xie D. Replicated studies of two randomized trials of angiotensin-converting enzyme inhibitors: further empiric validation of the 'prior event rate ratio' to adjust for unmeasured confounding by indication. Pharmacoepidemiol Drug Saf. 2008;17(7):671-685.
3. Tannen RL, Weiner MG, Xie D. Use of primary care electronic medical record database in drug efficacy research on cardiovascular outcomes: comparison of database and randomised controlled trial findings. BMJ. 2009;338:b81.
4. Yu M, Xie D, Wang X, Weiner MG, Tannen RL. Prior event rate ratio adjustment: numerical studies of a statistical method to address unrecognized confounding in observational studies. Pharmacoepidemiol Drug Saf. 2012;21(S2):60-68.
5. Uddin MJ, Groenwold RH, van Staa TP, et al. Performance of prior event rate ratio adjustment method in pharmacoepidemiology: a simulation study. Pharmacoepidemiol Drug Saf. 2015;24(5):468-477.
6. Lin NX, Henley WE. Prior event rate ratio adjustment for hidden confounding in observational studies of treatment effectiveness: a pairwise cox likelihood approach. Stat Med. 2016;35(28):5149-5169.
7. Greenland S, Pearl J, Robins JM. Causal diagrams for epidemiologic research. Epidemiology. 1999;10:37-48.
8. Pearl J. Probabilistic Reasoning in Intelligent Systems: Networks of Plausible Inference. Amsterdam, The Netherlands: Elsevier; 2014.
9. Young-Xu Y, Van Aalst R, Mahmud SM, et al. Relative vaccine effectiveness of high-dose versus standard-dose influenza vaccines among veterans health administration patients. J Infect Dis. 2018217:1718-1727.
10. RC Team. R: A Language and Environment for Statistical Computing. Vienna, Austria: R Foundation for Statistical Computing; 2015.
11. Lash TL, Fox MP, Fink AK. Applying Quantitative Bias Analysis to Epidemiologic Data. New York, NY: Springer Science & Business Media; 2011.
12. DiazGranados CA, Dunning AJ, Kimmel M, et al. Efficacy of high-dose versus standard-dose influenza vaccine in older adults. N Engl J Med. 2014;371(7):635-645.
13. Andrew MK, Shinde V, Ye L, et al. The importance of frailty in the assessment of influenza vaccine effectiveness against influenza-related hospitalization in elderly people. J Infect Dis. 2017;216(4):405-414.
14. DiazGranados CA, Dunning AJ, Robertson CA, Talbot HK, Landolfi V, Greenberg DP. Efficacy and immunogenicity of high-dose influenza vaccine in older adults by age, comorbidities, and frailty. Vaccine. 2015;33(36):4565-4571.
15. Gill TM, Gahbauer EA, Han L, Allore HG. The relationship between intervening hospitalizations and transitions between frailty states. J Gerontol A Biol Sci Med Sci. 2011;66(11):1238-1243.
16. Mullooly JP, Bridges CB, Thompson WW, et al. Influenza- and RSV-associated hospitalizations among adults. Vaccine. 2007;25(5):846-855.
17. McGraw KO, Wong SP. A common language effect size statistic. Psychol Bull. 1992;111(2):361.
18. Hodges JL Jr, Lehmann EL. Estimates of location based on rank tests. Ann Math Stat. 1963;598-611.

SUPPORTING INFORMATION

Additional supporting information may be found online in the Supporting Information section at the end of the article.
APPENDIX A

With specific reference to the HD influenza study of Young-Xu et al., we are now prepared to consider scenarios wherein we apply progressively more restrictive constraints on the prior ranges of the input parameters. All ranges are tightened progressively by incorporating the following additional conditions:

\[ P(Y_2 = y_2|C_2, Y_1, X) = r_{y_2} \cdot \begin{cases} F_{c\rightarrow y_2}, & \text{if } C_2 = c_2 \\ 1, & \text{if } C_2 = \overline{c}_2 \end{cases} \cdot \begin{cases} F_{y_1\rightarrow y_2}, & \text{if } Y_1 = y_1 \\ 1, & \text{if } Y_1 = \overline{y}_1 \end{cases} \cdot \begin{cases} F_{HD\rightarrow y_2}, & \text{if } X = HD \\ F_{SD\rightarrow y_2}, & \text{if } X = SD. \end{cases} \]

where

\[ r_{y_2} = \frac{F_{y_1\rightarrow y_2}}{F_{HD\rightarrow y_2} \cdot F_{SD\rightarrow y_2}} \]

and

\[ rVE_{HD} = 100\% \cdot (1 - F_{HD,rel}). \]

If, in the absence of the attenuation, \( F_{c\rightarrow y_2} = F_{c_{\text{rel}} ightarrow y_1} \), then with attenuation factor \( f > 1 \),

\[ F_{c\rightarrow y_2} = f \cdot F_{c_{\text{rel}} ightarrow y_1} > F_{c_{\text{rel}} ightarrow y_1}. \]

(21)

APPENDIX B

We begin with minimal assumptions about the input parameters (Analysis 1) and then consider a series of scenarios wherein we apply progressively more restrictive constraints on the prior ranges of the input parameters. All ranges are
FIGURE B1  Results of probabilistic bias analysis to assess the true relative effectiveness of high-dose (HD) versus standard-dose (SD) influenza vaccine, $rVE_{HD}$, for the scenarios in Table B1 [Colour figure can be viewed at wileyonlinelibrary.com]

taken as uniform, and in all scenarios, we take $r_{c,a} \in [0.25,0.75]$, $F_{c,a} \rightarrow y_1 \in [1,10]$, and $F_{y_1 \rightarrow y_2} \in [1,10]$. For each analysis, we report the distributions of $rVE_{HD, true}$ and compare it to $rVE_{HD, PERR}$, the PERR estimate derived by Young-Xu et al. Specifically, we wish to quantify to what degree the PERR over/underestimates the true treatment effect. We do so using two different metrics: the CLES\textsuperscript{17}) and the two-sample Hodges-Lehmann estimator for the difference between two populations.\textsuperscript{18} The CLES gives the probability that a sample drawn from the distribution of $rVE_{HD, PERR}$ is greater than a sample drawn from the distribution of $rVE_{HD, true}$. In other words, it gives the probability that PERR overestimates the true effect size. The two-sample Hodges-Lehmann estimator is a nonparametric estimator of the median difference between a pair of samples drawn from the two distributions. The setups and results of the simulations are given in Table B1. Results are shown graphically in Figure B1.

APPENDIX C

INTERVIEW SURVEY: HIGH-DOSE VACCINE ALLOCATION IN THE VETERANS HEALTH ADMINISTRATION

BACKGROUND

The objective of this survey study was to understand the contributing factors to the variations in the HD influenza vaccine coverage among VHA facilities and to gain insight into the decision-making process for determining eligibility for and access to HD vaccine.

METHODS

We used HD vaccine proportion to measure facilities’ HD vaccine coverage. The numerator for the measure was calculated as the number of patients aged 65 and older who received the HD influenza vaccine during the 2014-2015 influenza season and the denominator was the total number of patients 65 and older who received either the HD or SD influenza vaccine during the 2014-2015 influenza season. Administration of the flu vaccine, as well as the vaccine type, were
TABLE B1  Setup and results of the set of seven probabilistic bias analyses (PBA) conducted on the Veterans Health Administration study of Young-Xu et al.9 Starting with minimal assumptions about the relationships among $C_1$, $C_{1b}$, $C_2$, $Y_1$, $X$, and $Y_2$, we add assumptions (described in the leftmost column) one by one and apply the corresponding constraints on the input parameters. Cells corresponding to tightened constraints are shown in light gray, and darker gray for the one instance of a constraint further tightened.

| Assumptions                                                                 | PBA input parameters | Results                                                                 |
|----------------------------------------------------------------------------|----------------------|------------------------------------------------------------------------|
| RR of direct effect of baseline hospitalization on probability of HD receipt ($F_{1Y}$) | Probability that frail subject (baseline) becomes nonfrail (observation) ($P_{C2|C1b}$) | Relationship between frailty effect on hospitalization in observation and baseline period: ($f \equiv \frac{F_{C1b|Y}}{F_{C1b|Y1}}$) | RR of effect of baseline hospitalization on baseline frailty: ($F_{Y1 \rightarrow C1b}$) | Probability that nonfrail subject (baseline) becomes frail (observation) scaled by baseline frailty rate ($F_{new} \equiv \frac{F_{new}}{F_{1Y}}$) | $r^{VE}_{HD\text{true}}$ (%) | Comparison to $r^{VE}_{HD\text{PERR}}$ ($\%$) | Two-sample Hodges-Lehmann estimate of median difference (%) (positive values are PERR overestimates) |
| 1) Minimal assumptions                                                     | [0.1, 10]            | [0, 1]                                                                 | no relationship                                           | [1, 10] | [0, 1] | $-31(-184; 30)$ | 0.957 | 57 |
| 2) No direct effect of baseline hospitalization on probability of receiving HD | 1                    | [0, 1]                                                                 | no relationship                                           | [1, 10] | [0, 1] | $-10(-46; 19)$ | 0.968 | 34 |
| 3) Subjects do not recover from frailty                                    | 1                    | 0                                                                     | no relationship                                           | [1, 10] | [0, 1] | 0(-37; 26) | 0.927 | 26 |
| 4) Frailty effect on hospitalization is at least as strong in observation as baseline period | 1                    | 0                                                                     | [1, 10]                                                 | [1, 10] | [0, 1] | 9(-18; 37) | 0.814 | 16 |
| 5) In baseline period, frailty effect on hospitalization is at least as strong as hospitalization effect on frailty | 1                    | 0                                                                     | [1, 10]                                                 | [1, $F_{cO \rightarrow Y1}$] | [0, 1] | 15(-17; 57) | 0.682 | 9  |
| 6) Previously nonfrail subjects do not become frail in observation period   | 1                    | 0                                                                     | [1, 10]                                                 | [1, $F_{cO \rightarrow Y1}$] | 0 | 26(-12; 68) | 0.459 | -1 |
| 7) In baseline period, hospitalization has no effect on frailty             | 1                    | 0                                                                     | [1, 10]                                                 | 1 | 0 | 38(-13; 74) | 0.245 | -14 |
determined by CPT codes (HD: 90662, SD: 90655-90659, Q2034-Q2039) from VHA EMRs. VHA medical centers were stratified into four groups according to HD vaccine proportion: 0%-4%, 5%-29%, 30%-69%, and 70%-100%.

Initially, 10 facilities were randomly selected from each of the four HD vaccine proportion groups. For each site, we randomly selected and invited one nurse infection preventionist at a time to participate in a 10-15-minute telephone interview. If the interviewee was unable to provide all requested information at the time of the interview, follow-up interviews were performed with the individual, and/or additional facility personnel, such as other infection preventionists or pharmacists. If no response to the initial invitation(s) was received within a specified amount of time, another facility from within the same HD vaccine proportion group was selected at random, and the process repeated.

The content of the interview focused on the two most recent influenza seasons: 2015-2016 and 2016-2017. Twenty-two questions were organized into the following four areas.

1. HD vaccination policy (n = 7)
2. Defining criteria for a high-risk patient (n = 6)
3. Contra-indication for the HD vaccine (n = 3)
4. Quantity of HD vaccine (n = 6)

Responses were summarized as frequencies at the HD proportion group level. Where possible, numbers were imputed based on the type of response provided. For example, for the purpose of calculating percentages of HD vaccine used, we were able to ascertain the number ordered and the number used if percentages and at least one quantity were reported. Due to the small sample size and descriptive nature of this study, no statistical tests were performed.

RESULTS

Data were collected from 34 employees at 25 facilities (Table C1). Sixteen (64%) of the responding facilities provided complete information requested in the survey.

| Proportion of HD vaccine administered* | Selected VHA Medical Centers | Contacted Interviewees (potential) | Data Collected Interviewees (consented) |
|--------------------------------------|-----------------------------|-----------------------------------|---------------------------------------|
| A: 0%-4%                             | 41                          | 19                                | 36                                    | 6                                      | 9                                      |
| B: 5%-29%                            | 17                          | 17                                | 37                                    | 8                                      | 9                                      |
| C: 30%-69%                           | 12                          | 12                                | 27                                    | 6                                      | 8                                      |
| D: 70%-100%                          | 12                          | 12                                | 25                                    | 5                                      | 8                                      |
| TOTAL                                | 82                          | 60                                | 118                                   | 25                                     | 34                                     |

* During the 2014-2015 season; VHA: Veterans Health Administration.

| Proportion of HD vaccine administered* | Season 1: 2015-2016** | Season 2: 2016-2017** | Season 2-Season 1 Difference*** |
|--------------------------------------|------------------------|------------------------|---------------------------------|
| N Ordered                            | Used                   | % Used                | Ordered                         | Used                   | % Used                | Ordered                         | Used                   |
| A: 0%-4%                             | 6                      | 16150                 | 12753 | 79.0% | 6                      | 29400                 | 24208 | 82.3% |
| B: 5%-29%                            | 5                      | 29100                 | 26806 | 92.1% | 3                      | 10050                 | 9950  | 99.0% |
| C: 30%-69%                           | 6                      | 11200                 | 1075  | 96.0% | 6                      | 18000                 | 16371 | 91.0% |
| D: 70%-100%                          | 3                      | 23000                 | 19993 | 86.9% | 4                      | 42290                 | 41356 | 97.8% |
| TOTAL                                | 20                     | 69370                 | 60627 | 87.4% | 19                     | 99740                 | 91885 | 92.1% |

* During the 2014-2015 season.
** Includes those facilities reporting ordered and used amounts.
*** Includes those facilities reporting ordered and/or used amounts for both seasons.
HD vaccine ordered and used

Nine (36%) facilities provided partial data for either the quantity of HD vaccine ordered or percentage used, or were able to provide the information for one season only. The ordered, used and percentage HD used varied greatly across the four groups and within each group (Table C2). Only 8 out of 20 facilities (40%) and 10 out of 19 (53%) reported utilizing 100% of the ordered HD in 2015-2016 and 2016-2017, respectively. Of the 17 facilities that reported ordered HD quantities for both seasons, 10 (59%) increased, 1 (6%) decreased, and 6 (35%) did not alter the amount ordered for the following 2016-2017 influenza season as compared to 2015-2016. Also, 40% (N = 10) increased the amount of HD ordered for the most recent season, 2017-2018, as compared to 2015-2016 and 2016-2017.

Decision making process for HD vaccine acquisition

Primary decision-makers for the quantity of seasonal HD supply reported were similar across the four groups as pharmacy and/or a multidisciplinary committee consisting of representatives from various specialties, most commonly Infection Control and Infectious Diseases (Table C3). In seven (28%) facilities, pharmacy was a sole decision-maker for determining the amount of HD to be ordered for a season.

Overall, 10 (40%) facilities reported a shortage or inability to meet the demand for HD vaccine, and, for some, this occurred despite reported unused HD vaccine at the end of the season (N = 3). In these instances, the leftover doses were attributed to strict adherence to the criteria for HD administration (N = 1), extra supply received from other facilities (N = 1), and for one, no explanation was offered. Of the 12 facilities that reported unused HD, the remaining 9 (75%) reported no shortage or unmet demand. Reasons for the surplus cited included staff unaware of HD availability (N = 3), strict adherence to the criteria for HD administration (N = 1), lack of demand (N = 1), low vaccination rates overall (N = 1), possibly poor documentation of administered HD (N = 1), and for two, no explanation was offered.

The cost of HD vaccine (N = 2), lack of conclusive evidence (N = 5), and unused doses of HD in the prior season (N = 2) were the reported barriers to increasing HD supply for the future seasons. A common theme among the surveyed infections prevention and pharmacists was the perception of a lack of clear guidance from the Centers for Disease Control and Prevention (CDC) or in the scientific literature regarding administration of HD vaccine.

Criteria, policies, and practices for HD administration

Twenty (80%) of surveyed facilities have a standing nursing order for HD administration and the use of such a practice varied from 100% for Group A to 67% for Group C (Table C4). Similarly, a majority or 18 (72%) have a facility-wide policy on HD encompassing: age alone (N = 13); a combination of age and presence of certain comorbidities (N = 4); or positive HIV status (N = 1). Ten (40%) facilities have department-specific policies or practices for: Home-Based Primary Care (N = 2), acute care (N = 3), and Community Living Center (CLC)-residing (N = 8), patients, as well as geriatric (N = 1), Infectious Diseases (N = 1), and HIV (N = 1) clinics. Provider discretion for HD administration on an individual basis despite the presence of facility-wide or department-specific policies was reported by 20 (80%) of facilities, and, furthermore, for 18 (72%), respondents reported that providers specifically target patients they determine to be at high-risk not otherwise covered in an existing policy.

Overall, 14 (56%) reported a facility-wide policy, 6 (24%) department-specific policies, and 4 (16%) a combination of both facility-wide and department-specific policies, while 1 (4%) reported relying solely on provider’s discretion for administering HD in patients who are aged 65 years and older. All facilities in the highest HD proportion group (D) reported using a facility-wide policy on the basis of age alone and no department-specific policies; however, 60% (N = 3) of these reported that providers are able to use their discretion to target high-risk patients if they do not meet the age criterion.

Defining high-risk in the setting of HD vaccination varied from one facility to another: 22 (88%) consider advanced age (defined as 65+ (N = 20), 80+ (N = 1) or 85+ (N = 1)) to be a criterion, which aligns with the policies described above (Table C5). In 18 (72%) of these 22 facilities, meeting the age criterion alone was sufficient to be considered at high-risk, whereas for four (16%), such a consideration necessitated a combination of advanced age and the presence of certain chronic conditions such as diabetes, chronic obstructive pulmonary disease, chronic heart disease, or immunocompromised status. In addition to these, other patient criteria reported included, but were not limited to positive HIV status, CLC residency or being seen in a high-risk clinic.

Contraindications for HD administration

Eleven (44%) of the surveyed facilities reported contra-indications for HD administration (Table C6). Two (8%) reported that a recent pneumonia hospitalization could be a reason to give a SD instead of HD vaccine to an individual. The most commonly reported reason for delay or avoidance of HD vaccination was prior history of allergic reaction to an influenza vaccine or its components (N = 8). Presence of fever was cited as the second most common contra-indication (N = 5), followed by already immunized (N = 2), and history of Guillain-Barre syndrome (N = 2).
### TABLE C3  
Mechanisms of acquiring high dose (HD) influenza vaccine among study participants (Veterans Health Administration facilities) for the 2015-2016 and 2017-2018 seasons by group

| Characteristic                        | Proportion of HD vaccine administered during the 2014-2015 season | Total |
|---------------------------------------|---------------------------------------------------------------|-------|
|                                       | A: 0%-4% | B: 5%-29% | C: 30%-69% | D: 70%-100% | N = 25 |
| HD quantity decision makers           |          |           |             |              |       |
| Pharmacy                              | N = 6    | N = 8     | N = 6       | N = 5        |       |
|                                       | 5 (83.3%) | 6 (75.0%) | 4 (66.7%)   | 3 (60.0%)    | 18 (72.0%) |
| Infection Control                     |          |           |             |              |       |
|                                       | 1 (16.7%) | 2 (25.0%) | 1 (16.7%)   | 1 (20.0%)    | 5 (20.0%)  |
| Multidisciplinary committee           |          |           |             |              |       |
| Department Chiefs/Individual Providers| N = 6    | N = 8     | N = 6       | N = 5        |       |
|                                       | 2 (33.3%) | 2 (25.0%) | 2 (33.3%)   | 1 (20.0%)    | 7 (28.0%)  |
| Barriers to ordering                  |          |           |             |              |       |
| Cost                                  | N = 6    | N = 8     | N = 6       | N = 5        |       |
|                                       | 1 (16.7%) | 1 (12.5%) | 0           | 0            | 2 (8.0%)   |
| Lack of evidence                      | N = 6    | N = 8     | N = 6       | N = 5        |       |
|                                       | 0        | 3 (37.5%) | 1 (16.4%)   | 1 (20.0%)    | 5 (20.0%)  |
| Prior waste                           | N = 6    | N = 8     | N = 6       | N = 5        |       |
|                                       | 1 (16.7%) | 1 (12.5%) | 0           | 0            | 2 (8.0%)   |
| Shortage in at least one season?      | N = 6    | N = 8     | N = 6       | N = 5        |       |
|                                       | 2 (33.3%) | 3 (42.9%) | 3 (50.0%)   | 3 (60.0%)    | 10 (40.0%) |
| Unused vaccine in at least one season?| N = 6    | N = 8     | N = 6       | N = 5        |       |
|                                       | 4 (66.7%) | 2 (28.6%) | 2 (33.3%)   | 3 (60.0%)    | 11 (44.0%) |
| Reason for unused vaccine             |          |           |             |              |       |
| Staff unaware of supply               | N = 6    | N = 8     | N = 6       | N = 5        |       |
|                                       | 2 (33.3%) | 0         | 1 (16.7%)   | 0            | 3 (12.0%)  |
| Adherence to administration criteria  | N = 6    | N = 8     | N = 6       | N = 5        |       |
|                                       | 1 (16.7%) | 0         | 0           | 1 (20.0%)    | 2 (8.0%)   |
| Other (ie, extra supply received from other facility, lack of demand, low vaccination levels, and poor documentation) | N = 6 | N = 8 | N = 6 | N = 5 |       |
|                                       | 1 (16.7%) | 1 (12.5%) | 1 (16.7%)   | 1 (20.0%)    | 4 (16.0%)  |
| Ordered more for 2017/2018 season     | N = 6    | N = 8     | N = 6       | N = 5        |       |
|                                       | 3 (60.0%) | 3 (42.9%) | 1 (25.0%)   | 3 (60.0%)    | 10 (40.0%) |
**TABLE C4**  Policies and practices for distributing high dose (HD) influenza vaccine among study participants (Veterans Health Administration facilities) for the 2015-2016 and 2017-2018 seasons by group

| Characteristic                                | Proportion of HD vaccine administered during the 2014-2015 season | Total |
|-----------------------------------------------|---------------------------------------------------------------|-------|
|                                               | A: 0%-4%  B: 5%-29%  C: 30%-69%  D: 70%-100% |       |
|                                               | N = 6      | N = 8      | N = 6      | N = 5      | N = 25 |
| Standard nursing order/protocol               |                                                      |       |
| Applies?                                      | 6 (100%)   | 6 (75.0%)  | 4 (66.7%)  | 4 (80.0%)  | 20 (80.0%) |
| Facility-wide policy                          |                                                      |       |
| Applies?                                      | 6 (100%)   | 4 (50.0%)  | 3 (50.0%)  | 5 (100%)   | 18 (72.0%) |
| Age (65+)                                     | 6 (100%)   | 3 (37.5%)  | 3 (50.0%)  | 5 (100%)   | 17 (68.0%) |
| Immuno-compromised/HIV Chronic                | 1 (16.7%)  | 3 (37.5%)  | 0          | 0          | 4 (16.0%) |
| Facility-wide policy                          |                                                      |       |
| CLC/HBPC                                      | 1 (16.7%)  | 1 (12.5%)  | 1 (16.7%)  | 0          | 3 (12.0%) |
| Acute care                                    | 1 (16.7%)  | 2 (25.0%)  | 0          | 0          | 3 (12.0%) |
| Specialty Clinics                             | 0          | 3 (37.5%)  | 0          | 0          | 3 (12.0%) |
| Department-specific policy/practice           |                                                      |       |
| Applies?                                      | 2 (33.3%)  | 2 (33.3%)  | 3 (50.0%)  | 0          | 10 (40.0%) |
| CLC/HBPC                                      | 1 (16.7%)  | 5 (62.5%)  | 3 (50.0%)  | 0          | 9 (36.0%) |
| Acute care                                    | 1 (16.7%)  | 2 (25.0%)  | 0          | 0          | 3 (12.0%) |
| Specialty Clinics                             | 0          | 3 (37.5%)  | 0          | 0          | 3 (12.0%) |
| Provider discretion                           |                                                      |       |
| Applies?                                      | 5 (83.3%)  | 7 (87.5%)  | 5 (83.3%)  | 3 (60.0%)  | 20 (80.0%) |
| MD                                            | 5 (83.3%)  | 7 (87.5%)  | 5 (83.3%)  | 3 (60.0%)  | 20 (80.0%) |
| NP/PA                                         | 4 (66.7%)  | 7 (87.5%)  | 4 (66.7%)  | 3 (60.0%)  | 18 (72.0%) |
| RN                                            | 2 (33.3%)  | 6 (75.0%)  | 1 (16.7%)  | 1 (20.0%)  | 10 (40.0%) |
| LPN                                           | 0          | 1 (12.5%)  | 0          | 0          | 1 (4.0%)  |
| Provider discretion                           |                                                      |       |
| Target patients at high-risk not covered by policies | 6 (100%)   | 6 (75.0%)  | 3 (50.0%)  | 3 (60.0%)  | 18 (72.0%) |
| Characteristic                                      | Proportion of HD vaccine administered during the 2014-2015 season | Total |
|---------------------------------------------------|---------------------------------------------------------------|-------|
|                                                   | A: 0%-4%           | B: 5%-29%          | C: 30%-69%         | D: 70%-100%         | N = 25 |
| N = 6                                            | N = 8             | N = 6              | N = 5              |
| 65+                                               | 22 (88.0%)        | 22 (88.0%)         | 22 (88.0%)         | 22 (88.0%)         |       |
| Age 80+                                           | 1 (4.0%)          | 1 (4.0%)           | 1 (4.0%)           | 1 (4.0%)           |       |
| 85+                                               | 1 (4.0%)          | 1 (4.0%)           | 1 (4.0%)           | 1 (4.0%)           |       |
| Home-Based Primary Care patient                   | 2 (8.0%)          | 2 (8.0%)           | 2 (8.0%)           | 2 (8.0%)           |       |
| Inpatient (acute care)                            | 1 (4.0%)          | 1 (4.0%)           | 1 (4.0%)           | 1 (4.0%)           |       |
| Community Living Center resident                  | 4 (16.0%)         | 4 (16.0%)          | 4 (16.0%)          | 4 (16.0%)          |       |
| Being seen in high risk clinic (eg, geriatrics, Infectious Diseases, HIV, pulmonary, nephrology, oncology, and rheumatology) | 3 (12.0%)         | 3 (12.0%)          | 3 (12.0%)          | 3 (12.0%)          |       |
| Immunocompromised                                 | 9 (36.0%)         | 9 (36.0%)          | 9 (36.0%)          | 9 (36.0%)          |       |
| HIV positive                                      | 3 (12.0%)         | 3 (12.0%)          | 3 (12.0%)          | 3 (12.0%)          |       |
| HIV/AIDS w/low CD-4 meter                         | 1 (4.0%)          | 1 (4.0%)           | 1 (4.0%)           | 1 (4.0%)           |       |
| Renopathic condition                              | 2 (8.0%)          | 2 (8.0%)           | 2 (8.0%)           | 2 (8.0%)           |       |
| on dialysis                                       | 2 (8.0%)          | 2 (8.0%)           | 2 (8.0%)           | 2 (8.0%)           |       |
| Diabetes                                          | 1 (4.0%)          | 1 (4.0%)           | 1 (4.0%)           | 1 (4.0%)           |       |
| Asthmatic                                         | 2 (8.0%)          | 2 (8.0%)           | 2 (8.0%)           | 2 (8.0%)           |       |
| Respiratory issues                                | 2 (8.0%)          | 2 (8.0%)           | 2 (8.0%)           | 2 (8.0%)           |       |
| Asthmatic                                         | 2 (8.0%)          | 2 (8.0%)           | 2 (8.0%)           | 2 (8.0%)           |       |
| Chronic pulmonary condition                       | 4 (16.0%)         | 4 (16.0%)          | 4 (16.0%)          | 4 (16.0%)          |       |
| Chronic obstructive pulmonary disease             | 3 (12.0%)         | 3 (12.0%)          | 3 (12.0%)          | 3 (12.0%)          |       |
| Cardiovascular condition                          | 5 (20.0%)         | 5 (20.0%)          | 5 (20.0%)          | 5 (20.0%)          |       |
| Chronic obstructive pulmonary disease             | 4 (16.0%)         | 4 (16.0%)          | 4 (16.0%)          | 4 (16.0%)          |       |
| Heart disease                                     | 2 (8.0%)          | 2 (8.0%)           | 2 (8.0%)           | 2 (8.0%)           |       |
| Congestive heart failure                          | 3 (12.0%)         | 3 (12.0%)          | 3 (12.0%)          | 3 (12.0%)          |       |
| Neurological condition                            | 1 (4.0%)          | 1 (4.0%)           | 1 (4.0%)           | 1 (4.0%)           |       |
| Neuropathic condition                             | 1 (4.0%)          | 1 (4.0%)           | 1 (4.0%)           | 1 (4.0%)           |       |
| Other/unspecified chronic condition               | 1 (4.0%)          | 1 (4.0%)           | 1 (4.0%)           | 1 (4.0%)           |       |
| Blood-borne infection                             | 1 (4.0%)          | 1 (4.0%)           | 1 (4.0%)           | 1 (4.0%)           |       |
| Flu in the previous season                        | 1 (4.0%)          | 1 (4.0%)           | 1 (4.0%)           | 1 (4.0%)           |       |
### TABLE C6
Contra-indication criteria for high dose (HD) influenza vaccination administration among study participants (Veterans Health Administration facilities) for the 2015-2016 and 2017-2018 seasons by group

| Characteristic                                              | Proportion of HD vaccine administered during the 2014-2015 season |
|-------------------------------------------------------------|---------------------------------------------------------------|
|                                                             | A: 0%-4% B: 5%-29% C: 30%-69% D: 70%-100% Total              |
|                                                             | N = 6 N = 8 N = 6 N = 5 N = 25                               |
| Reported contra-indication                                  |                                                             |
| History of allergic reaction to influenza vaccine or its components | 3 (50.0%) 3 (37.5%) 3 (50.0%) 2 (40.0%) 11 (44.0%)          |
| History of allergic reaction to eggs                        | 3 (50.0%) 1 (12.5%) 2 (33.3%) 2 (40.0%) 8 (32.0%)          |
| Allergy to latex or thimerosal                              | 1 (16.7%) 1 (12.5%) 0 0 1 (4.0%)                            |
| Already immunized                                           | 1 (16.7%) 0 1 (16.7%) 0 2 (8.0%)                            |
| History of Guillain-Barre syndrome                          | 1 (16.7%) 0 0 1 (20.0%) 2 (8.0%)                            |
| Not feeling well                                            | 1 (16.7%) 0 0 0 1 (4.0%)                                   |
| Moderate to severe acute illness                            | 1 (16.7%) 2 (25.0%) 1 (16.7%) 1 (20.0%) 5 (20.0%)          |
| Presence of fever                                           | 1 (16.7%) 1 (12.5%) 0 0 2 (8.0%)                            |
| Chemotherapy of radiation therapy                           | 1 (16.7%) 1 (12.5%) 0 0 2 (8.0%)                            |
| Pre-op or pre-procedure for invasive procedures/surgeries   | 1 (16.7%) 0 0 0 1 (4.0%)                                   |
| Patient being administered Coumadin                         | 0 1 (12.5%) 0 0 1 (4.0%)                                   |
| Hospice care                                                | 0 1 (12.5%) 0 0 1 (4.0%)                                   |
| Person without capacity to make an informed decision        | 0 1 (12.5%) 0 0 1 (4.0%)                                   |
| Physician discretion                                        | 0 0 1 (16.7%) 0 1 (4.0%)                                   |
| Recent pneumonia hospitalization                            | 0 0 2 (33.3%) 0 2 (8.0%)                                   |