Research Article

Computational Modeling of Desiccation Properties (CW, LS, and VS) of Waste-Based Activated Ash-Treated Black Cotton Soil for Sustainable Subgrade Using Artificial Neural Network, Gray-Wolf, and Moth-Flame Optimization Techniques

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Artificial neural network (ANN), gray-wolf, and moth-flame optimization (GWO and MFO) techniques have been used in this research work to predict the effect of activated sawdust ash (ASDA) on the crack width (CW), linear shrinkage (LS), and volumetric shrinkage (VS) of a black cotton soil utilized as a subgrade material. Problematic soils or black cotton soils are not good pavement foundation materials except that they are pretreated in order to meet the basic strength characteristics required for roads in Nigeria. Due to this reason, there has been ongoing research to evaluate the best practices in which black cotton soils can be favorably utilized in earthwork construction. On the other hand, there is a huge concern on the solid waste management system in the wood processing environment and the recycling of sawdust into ash and its reuse as an alternative binder has offered a sustainable disposal system. The work tries to use AI-based techniques to predict the crack and shrinkage behaviors of BCS treated with saw dust ash activated with alkali materials. There was appreciable improvement in the shrinkage and crack parameters over the 30-day drying period due to the addition of ASDA. The intelligent model results showed that the three techniques successfully predicted the CW, LS, and VS with a performance accuracy above 90%, while ANN produced the minimal error in performance outperforming the other techniques. Sensitivity study showed that the drying time (T) was the most influential of the studied parameter. Hence, soil stabilization has shown its potential system of waste management in the wood processing industry.

1. Introduction

The swell-shrink cycle is a phenomena exhibited by black cotton soils and other problematic soils when exposed to moisture either as a foundation material subjected hydraulically bound conditions or a superstructural material exposed to moisture ingress through suction or migration from runoff. Due to this behavior, black cotton soils do not support foundation loads except they are pretreated to meet the minimum requirement for pavement subgrade. The handling and utilization of BCS is a worrisome procedure due to the erratic and unpredictable state of the soils. There have been successful stabilization procedures recorded with the use of BCS and agroindustrial-based waste materials added as cementing admixtures in a soil stabilization protocol [1]. However, there seems to be a serious concern due to multiple visits to the laboratory to generate data needed for earthwork designs and construction as well as
infrastructure performance evaluation exercise [2]. In order to overcome these challenges which also include the need for sophisticated laboratory equipment, there has been the deployment of smart and intelligent techniques based on the algorithms of AI-based predictive modeling in geotechnics and materials engineering. These AI-based techniques forecast engineering problems for use in future exercise to predict and to monitor the performance of built infrastructure. In addition to the AI-based techniques, e.g., ANN, GP, GEP, and EPR, there are also baseline regression methods like LMR or MLR, Pearson Regression, etc., which help to present the statistical analysis of multiple data collected for engineering analysis [1,2]. However, a group of methods have not been commonly used in the field of geosciences like gray-wolf optimization (GWO) and moth-fly optimization (MFO) algorithms. These novel methods are being applied in this research work in addition to artificial neural network (ANN) and linear multivariate regression (LMR) analysis to predict crack width, linear, and volumetric shrinkages of HSDA-treated BCS utilized as a subgrade material.

One of the most successful methods used to predict variance in distance dependence based on the linear composition of independent distance variables, dual or artificial, which was used by Pearson in 1908 is linear multivariate regression (LMR). The generalization of simple linear regression to more than one independent variable and a specific case of general linear models is limited to one dependent variable (Shakeri et al. 2020; [3]; Amini et al. 2021). Therefore, the general goal of this method is to obtain more information about the relationship between several independent or predictor variables and a dependent variable or criterion. The mentioned cases have led to the widespread use of this method to approximate problems in the field of engineering [3–6]; Amini et al., 2021; Monjezi et al., 2021). In this study, the dependent variables include Crack Width (CW), Volumetric Shrinkage (VS), and Linear Shrinkage (LS), which may depend on n independent variables (x). In general, a typical multiple regression formula is presented in the following format:

\[ C = \beta_0 + \beta_1 x_1 + \cdots + \beta_n x_n + \varepsilon, \]  

(1)

where \( \varepsilon \) is the error of the model; \( j = 0, 1, \ldots, n \) and \( \beta_j \) are the regression coefficients (Amini et al., 2021; Shakeri et al., 2020; [4]; Montgomery, 1992; [3]).

The gray-wolf algorithm, which is inspired by the natural life and hunting process of gray wolves, can be used to solve complex optimization problems. This algorithm has been proposed by Mirjalili et al. and has been used in many engineering issues [7–10]. Gray wolves have a social hierarchy, all of which are divided into four categories based on their objective values [11]; Mirjalili et al. 2014; [12,13]. The responsibility for decision-making (such as hunting and sleeping) rests with the leader of the wolf alpha group (a), and the second group that assists the alpha group in decision-making is the wolf beta (b) commanders. The subordinates of delta wolves (d) and in the lowest rank omega wolves (\( \omega \)) are those who follow the instructions of the dominant wolves (a, b, and \( \delta \)) in the evolution of the algorithm (see Figure 1). According to Figure 2, to update the position of wolves in the search space, you can see the position of wolves and prey and the parameters in the equations used (in 2–6). According to studies (Mirjalili et al. 2014; Xu et al. 2020; [13–15]) the gray-wolf algorithm uses siege, hunt, attack, and recovery steps to hunt prey.

For this purpose, the following mathematical representation is defined to mimic the siege behavior of gray wolves:

\[ \bar{D} = |\overrightarrow{C}.\overrightarrow{X}_p(t) - \overrightarrow{X}(t)|, \]  

(2)

\[ \overrightarrow{X}(t + 1) = \overrightarrow{X}_p(t) - \overrightarrow{A}.\overrightarrow{D}. \]  

(3)

In these relations, \( t \) indicates the common repetition, \( \overrightarrow{X}_p \) represents the prey position vector, and \( \overrightarrow{X} \) represents the gray-wolf position vector. \( \overrightarrow{A} \) (\( A = 2\overrightarrow{d}.\overrightarrow{r}_1 - \overrightarrow{r}_2 \)) and \( \overrightarrow{C} \) (\( C = 2.\overrightarrow{r}_2 \)) are coefficient vectors and are calculated from the following equations (Mirjalili et al., 2014).

In this regard, the vector \( \overrightarrow{r}_2 \) decreases from 2 to 0 during different iterations and the \( \overrightarrow{r}_1 \) and \( \overrightarrow{r}_2 \) vectors are random vectors in [0,1]. In GWO, it is assumed that alpha, beta, and delta wolves have better knowledge of the possible location of prey (Mirjalili et al., 2014). Therefore, omega wolves must update their positions according to alpha, beta, and delta as follows:

\[ \overrightarrow{B}_a = |\overrightarrow{C}_1.\overrightarrow{X}_a - \overrightarrow{X}|, \overrightarrow{B}_\beta = |\overrightarrow{C}_2.\overrightarrow{X}_\beta - \overrightarrow{X}|, \overrightarrow{B}_\delta = |\overrightarrow{C}_3.\overrightarrow{X}_\delta - \overrightarrow{X}|, \]  

(4)

\[ \overrightarrow{X}_a = \overrightarrow{X}_a - \overrightarrow{A}_1(\overrightarrow{B}_a), \overrightarrow{X}_\beta = \overrightarrow{X}_\beta - \overrightarrow{A}_2(\overrightarrow{B}_\beta), \overrightarrow{X}_\delta = \overrightarrow{X}_\delta - \overrightarrow{A}_3(\overrightarrow{B}_\delta), \]  

(5)

\[ \overrightarrow{X}(t + 1) = \frac{\overrightarrow{X}_a + \overrightarrow{X}_\beta + \overrightarrow{X}_\delta}{3}. \]  

(6)

As shown by the algorithm trend in Figure 3, when all the wolves are moved (one iteration), the wolves (solutions) are reevaluated using the target function. The top three solutions become a, b, and d wolves, while the other wolves must update their position in the next iteration. These steps are repeated until the stop criterion is reached. The detail formulation of the GWO can be found in the literature (Mirjalili et al., 2014; Xu et al., 2020; [13]; Emary et al., 2020; [9]).

MFO is a swarm optimization algorithm based on the method of moving propellers (transverse direction) in nature. This algorithm is introduced by Mirjalili [17]. In MFO, the butterfly flies at a constant angle to the moon, and when a human creates artificial light, the butterflies see it and try to maintain the same angle with that light and fly in a straight line. Because such light is so close to the moon, maintaining the same angle as the light source creates an unhealthy or deadly spiral flight path for the butterflies (Figure 4). The initial, repeat, and stop criteria form the general framework of the MFO [17–20].
In the first stage, a population of butterflies is randomly generated by the MFO and calculates their appropriateness values. In the second stage, which is the iteration stage, the main function is performed and the butterflies move in the search space. In the third step, if the stop criterion is met, it returns correctly (see Figure 5). Conversely, if the stop criterion is not met, an incorrect item will be returned. As well as, the main method of updating the butterfly search space is the logarithmic helix [21–23].

Use (4) to update the position of each moth and simulate the flight mode of the moth.

\[ M_i = D_i e^{b t} \cdot \cos(2\pi t) + F_j, \]  

where \( D_i \) refers to the space between the \( i \)-th moth and the \( j \)-th flame (\( D_i = G_i - M_i \)), \( b \) indicates a fix to define the shape of the logarithmic spiral, and \( t \) indicates a random number between [-1, 1]. When \( t = -1 \), it means the distance between flame and moth is the closest, and when \( t = 1 \), it means the distance between them is the maximum. Equation (8) has been adopted to reduce the number of flames during each iteration by an adaptive linear method to improve the local extraction capacity of the moth in the next iteration [18,19,21,23–25]:

\[ \text{flame} = \text{round} \left( (N - 1) \frac{(N - 1)}{L} \right), \]  

where \( N \) is the maximum number of flames, \( I \) is the current number of iterations, and \( T \) indicates the maximum number of iterations. At the beginning of the iteration, the number of flames is \( N \), and the propellers update the position only at the end and around the best flame, which effectively increases the search capability of the MFO algorithm. More information on MFO programs and algorithms can be found in the literature (Mirjalili, 2015; [19–23,25]; Shehab et al., 2020; [24]).

Artificial neural networks inspired by the human nervous system are widely used today in various fields to predict

**Figure 1:** The social hierarchy of gray wolves [13].

**Figure 2:** The position update process of the gray-wolf algorithm (Mirjalili et al., 2014).

**Figure 3:** Flowchart of the GWO algorithm [16].
One of the most practical types of ANN models includes multilayer perceptron networks that have been used since the 1980s. The structure of these networks typically consists of three types of layers including the input layer, one or more hidden layers, and the output layer. According to existing studies ([3,28]; Amini et al., 2021), the use of only one hidden layer reduces the complexity of the model; however, there is no limit to the choice of the number of layers. Hypothetically, the GWO, MFO, and ANN techniques are more robust than other AI applications in geosciences.

MLP networks usually use different types of activation functions such as tansig, logsig, or purelin. In addition, the Levenberg–Marquardt algorithm is mostly used for network training in the forward-backend publishing process. More details are available in the literature [29,30]; Amini et al., 2021; [3,31,32]; Monjezi et al., 2021; [33].

2. Materials Preparation and Experimental Methods

2.1. Materials Preparation. The BCS was collected from Ikem Nvosio located on the coordinates of lat. 6.7799 and long. 7.7148. Figure 6(a) shows the BCS during the sun drying process. The soil was sandried for 5 days and kept in silo bags for use in the experiments. Figures 6(a) and 6(b) show the sawdust and sawdust during combustion to generate sawdust ash (SDA). The sawdust was collected from local wood processing factories at the Timber market where it is indiscriminately disposed, as a result of ineffective waste management system at the market. The scaling and blending of NaOH (aq) prepared at 8M (mol/L) for ecofriendly handling and NaSiO2 to formulate the alkali activator in line with the suggestions of Ashraf et al. [34] were also undertaken and reported by Onyelowe and Usungedo [35]. The two chemicals were mixed in the ratio of 1 : 1.5 liters of the aqueous NaOH which was produced bearing in mind its molar concentration, which eventually was used to estimate the number of moles of solute. This would not have been possible without determining the mass in grams of the flakes needed to produce 5 liters of the NaOH in solution bearing in mind its molar mass. With the solution of NaOH, the activator material was formulated and 5 wt % activator to the SDA was blended deeply with the SDA and allowed for 6 h. The end product of this process was HSDA (a composite binder formulated from biobased industrial solid waste reuse). Finally, the soil, BCS, and the HSDA (which meets the standard specification of ASTM C618 [36] and BS 8615–1 [37]) were stored for use in the stabilization process.

2.2. Experimental Methods. First, preliminary experiments were conducted in accordance with BS1377 [38] for the classification and characterization of test materials and they were particle size distribution (PSD) test, compaction test, Atterberg limits tests, free swell index test, and drying shrinkage test as reported by Onyelowe and Usungedo [35]. The following method was reported by Onyelowe and Usungedo [35]. Furthermore, the HSDA was used in the proportions of 3%, 6%, 9%, and 12% by weight of the dry...
sample to treat the BCS. The treated specimens were compacted using the standard proctor mold, extruded as shown in Figure 7, and placed in the oven to dry at 102°C for 30 days while the recording of the weight loss, height, and diameter continued for the desiccation duration. The average crack width of the specimens was also recorded using the Digital Vernier Calipers for the pretreated specimens for the 30 days. This stabilization process was conducted based on the requirements of BS1924 [39]. The volume ($V = \pi R^2 H$), bulk density ($BD = W/V$), linear shrinkage ($\frac{(H_o - H_t)}{H_o}$), and volumetric shrinkage ($\frac{(V_o - V_t)}{V_o}$) were estimated from measured experimental values. The multiple experimental data was collected and tabulated.

2.3. Generated Database and Statistical Analysis. In the present study, based on what is shown in Table 1, a comprehensive statistical indicators database consisting of 155 datasets with three output parameters and six input parameters has been prepared, which in this table shows the range of input and output parameters. Also, in Figure 8 and Table 2, the Pearson correlation for input and output data is shown schematically and in a matrix. Based on what has been done in previous studies ([3,4]; Monjezi et al., 2021) to find the best statistical relationship between input and output data, the data set was randomly divided into training and validation data. For this purpose, 70% of the data are considered as validation data and the remaining 30% as experimental data, and this division is the same for all methods used in this study.

3. Results and Discussions

3.1. Materials Characterization. In Figure 9, the particle size distribution of the BCS is presented with a 59.8% passing sieve number 200 (75 µm or 0.075 mm aperture). It can be observed that BCS is poorly graded. Figure 10 shows the propagation of cracks on the drying specimens. Table 3 shows the preliminary properties of the soil with MDD of 1.73 mg/m$^3$ obtained at an OMC of 11.2%; the Atterberg limits behavior of the BCS is presented with LL of 51.8%, PL of 16.4%, and PI of 37.7% ($> 17$%). It can be observed that the CBR is 7.6% (<10% for subgrade) and the SG is 2.285. The basic results show that the BCS belongs to an A-7 group of soil in accordance with the AASHTO classification. The soil can also be observed to be highly plastic. With the measured properties, it can be concluded that the BCS is problematic and does not have sufficient properties to be used as a subgrade material in its present condition.

3.2. Predicting with Multiple Linear Regression (MLR). Using the most widely used evaluation criteria in engineering (VAF, $R^2$, RMSE, and MAE), the performance of the models obtained in this study is compared in Table 4. Ideally, the RMSE and MAE values should be close to zero and the coefficient of determination ($R^2$), which is the correlation between the measured and predicted data, close to 1. Also, the VAF, which shows the difference between the variances, should be close to 1 or 100%. In fact, to find the best result, the four mentioned statistical parameters were selected as the best criteria for LMR, MFO, GWO, and ANN methods.
Table 1: Statistical indicators of input and output parameters.

| Statistics  | HSDA P(%) | Drying T(days) | Wt of spec. W(kg) | Height H(mm) | Diameter D(mm) | Volume V(ml) | Crack width CW(mm) | Volumetric shrinkage VS(%) | Linear shrinkage LS(%) |
|-------------|-----------|----------------|-------------------|--------------|----------------|--------------|---------------------|------------------------|------------------|
| Min         | 0.00      | 0.00           | 1.00              | 113.70       | 102.54         | 941.00       | 0.00                | 0.00                   | 0.00              |
| Max         | 12.00     | 30.00          | 1.56              | 115.50       | 105.00         | 1000.20      | 5.91                | 5.92                   | 1.56              |
| Mean        | 6.00      | 15.00          | 1.17              | 114.63       | 104.07         | 975.41       | 3.91                | 2.48                   | 0.74              |
| Std. deviation | 4.26    | 8.97           | 0.16              | 0.60         | 0.69           | 17.78        | 1.36                | 1.78                   | 0.51              |
| Variance    | 18.12     | 80.52          | 0.03              | 0.36         | 0.47           | 316.15       | 1.85                | 3.17                   | 0.26              |

\[
CW = 117.422 + (-0.036P) + (-0.024T) + (-3.411W) + (-0.74H) + (-0.025V) . 
\] (9)

\[
VS = 100.9 + (0.001P) + (-0.001T) + (-0.003W) + (0.002H) + (-0.101V),
\] (10)

\[
LS = 99.572 + (0.006P) + (-0.005T) + (-0.157W) + (-0.838H) + (-0.002V).
\] (11)

3.3. Predicting with GWO Method. In the first step, to design the GWO, determine the maximum number of repetitions \(I_{\text{max}}\) and the number of wolves to achieve the best performance of the GWO model. Therefore, the research was conducted to find the maximum number of optimal replications \(I_{\text{max}}\) and the number of wolves, which are listed in Table 5, and the prediction performance of the GWO model was investigated using RMSE. In this method, 70% (85 data) was used as training data and 30% (36 data) as test data and validated as presented in Figure 12.

Table 6 shows the results obtained from the optimal GWO model including \(R^2\), VAF, RMSE, and MAE for data training and testing, which are based on the highest \(R^2\), VAF, and the lowest MAE and RMSE. Figure 12 also shows a comparison between measured and predicted outputs values with the GWO model. In addition, the reduction of MSE during the implementation of the GWO process is shown in Figure 13.

3.4. Predicting with MFO Method. As mentioned earlier, in the MFO algorithm, it is assumed that the solutions are candidate for the moths and the variables of the problem are the position of the moths in space. Therefore, moths can fly in one-dimensional, two-dimensional, or three-dimensional space by changing their positional vectors. The difference between them is how they deal with and update each repetition. Flames can be considered flags or pins that are swallowed by moth when searching the search space. Therefore, each moth searches around a flag (flame) and updates it if it finds a better solution. With this mechanism, a moth never loses its best solution (Mirjalili, 2015).

According to what was said in the previous methods, the ratio of 70% (85 data) was used as educational data and 30% (36 data) that were randomly selected as test data. Tables 7 and 8 also summarize the MFO network parameters used in the present study to predict outputs and its performance, respectively.

The performance of the best models obtained for predicting outputs (CW, VS, and LS) with the MFO model is shown in Table 7 and the comparison between the measured and predicted values of these models is shown in Figure 14. The reduction of MSE during the MFO process is also shown in Figure 15.
Figure 8: Pearson’s schematic linear correlation regression of input and output data.

Table 2: Pearson’s correlation matrix of the input and output variables.

| Correlations | P  | T  | W  | H  | D  | V  | CW | VS | LS |
|--------------|----|----|----|----|----|----|----|----|----|
| P            | 1  | 0  | .303** | .239** | .139 | .169* | -.367** | -.166* | -.212** |
| T            | 0  | 1  | -.841** | -.930** | -.954** | -.957** | .815** | .957** | .926** |
| W            | .303** | -.841** | 1  | .860** | .838** | .854** | -.883** | -.854** | -.858** |
| H            | .239** | -.930** | .860** | 1  | .947** | .973** | -.892** | -.972** | -.992** |
| D            | .139 | -.954** | .838** | .947** | 1  | .996** | -.854** | -.996** | -.942** |
| V            | .169* | -.957** | .854** | .973** | .996** | 1  | -.875** | -.1000** | -.967** |
| CW           | -.367** | .815** | -.883** | -.892** | -.854** | -.875** | 1  | .874** | .881** |
| VS           | -.166* | .957** | -.854** | -.972** | -.996** | -.1000** | .874** | 1  | .966** |
| LS           | -.212** | .926v | -.858** | -.992** | -.942** | -.967v | .881** | .966** | 1    |

**Correlation is significant at the 0.01 level (2-tailed). * Correlation is significant at the 0.05 level (2-tailed).**
Figure 9: Particle size distribution of BCS.

Figure 10: HSDA-treated black cotton soil crack development under drying at 102°C [35].

Table 3: Basic properties of the BCS.

| Property | % Ps 200 | Nmc (%) | LL (%) | PL (%) | PI (%) | CBR (%) | MDD | OMC (%) | SG |
|----------|----------|---------|--------|--------|--------|---------|-----|---------|----|
| Value    | 59.8     | 18.1    | 51.8   | 16.4   | 37.7   | 7.6     | 1.73 mg/m³ | 11.2 | 2.285 |
Table 4: Performance indicator values for building MLR models for outputs.

| Variable | Train | | Test | |
|----------|-------|-------|-------|-------|
| CW       | R²    | VAF   | RMSE  | MAE   | R²    | VAF   | RMSE  | MAE   |
|          | 0.854 | 85.386| 0.558 | 0.450 | 0.884 | 87.686| 0.603 | 0.495 |
| VS       | 0.994 | 99.986| 0.125 | 0.124 | 0.999 | 99.899| 0.126 | 0.123 |
| LS       | 0.988 | 98.739| 0.598 | 0.596 | 0.982 | 98.108| 0.606 | 0.601 |

Figure 11: The values of R-squared for MLR models. (a) Crack width (CW), (b) volumetric shrinkage (VS), and (c) linear shrinkage (LS).

Table 5: The optimal GWO parameters for outputs.

| Parameter          | Common value |
|--------------------|--------------|
| Number of wolves   | 150          |
| Maximum number of iterations | 300          |
| a                  | Linearly increased from 2 to 0 |
3.5. Predicting with ANN Method. As the last effort for prediction crack width, volumetric shrinkage and linear shrinkage, and artificial neural network method was applied in present study. For this aim, a neural network with feedforward-backpropagation algorithm was considered. By examining different networks with one and two hidden layers containing several neurons; finally, a network with two hidden layers including 11 and 7 neurons in hidden layers, respectively, was obtained as optimum model with the best considered performance indicators for simultaneous predicting of CW, VS, and LS parameters. The schematic structure of the attained ANN model is illustrated in Figure 16.

Table 6: Performance indicator values for building GWO models for outputs (CW, VS, and LS).

| Variable | Train | Test |
|----------|-------|------|
|          | \(R^2\) | VAF | RMSE | MAE | \(R^2\) | VAF | RMSE | MAE |
| CW       | 0.927 | 92.708 | 0.349 | 0.235 | 0.916 | 91.512 | 0.434 | 0.266 |
| VS       | 0.999 | 99.972 | 0.029 | 0.021 | 0.999 | 99.866 | 0.067 | 0.034 |
| LS       | 0.985 | 98.543 | 0.062 | 0.033 | 0.985 | 98.543 | 0.062 | 0.033 |

Table 9 shows the considered parameters of optimal model and the values of considered performance indicators are given in Table 10. Finally, the relationship between measured values of CW, VS, and LS and predicted values by ANN are presented in Figure 17 for train and test data.

3.6. Discussion. Studies have shown that artificial intelligence approaches have been continuously developed due to the limitations of the laboratory environment, which has convinced researchers that they can use artificial intelligence methods to more accurately evaluate parameters than...
conventional approaches. The main purpose of this paper is to predict crack width (CW), volumetric shrinkage (VS), and linear shrinkage (LS) based on input parameters including HSDA (P), drying (T), Wt of spec. (W), height (H), diameter (D), and volume (V). To develop relationships, data collected from multiple experiments were first used to create a database between input and output data. Then, the best relationships between the outputs and each input were examined by comprehensive statistical analysis. Then, LMR, GWO, MFO, and ANN methods were used to predict CW, VS, and LS. The results of these methods were compared based on the highest $R^2$, VAF and the lowest values of MAE, RMSE for training and testing. The best values obtained for all methods based on statistical indices are given in Table 11.

According to Table 10, all methods show high accuracy in predicting CW, VS, and LS values due to the high

Table 7: The optimal MFO parameters for outputs (CW, VS, and LS).

| Parameter                        | Common value |
|----------------------------------|--------------|
| Number of search agents          | 250          |
| Number of moths (population)     | 60           |
| Maximum number of iterations     | 300          |

Table 8: Performance indicator values for building MFO models for outputs (CW, VS, and LS).

|   | Train |           |       |       | Test |       |       |
|---|-------|-----------|-------|-------|------|-------|-------|
|   | $R^2$ | VAF       | RMSE  | MAE   | $R^2$ | VAF   | RMSE  | MAE   |
| CW| 0.926 | 92.556    | 0.352 | 0.262 | 0.902 | 89.876| 0.477 | 0.341 |
| VS| 0.994 | 99.432    | 0.131 | 0.106 | 0.989 | 98.981| 0.186 | 0.133 |
| LS| 0.989 | 98.864    | 0.053 | 0.032 | 0.982 | 98.200| 0.069 | 0.041 |

Figure 13: MSE calculated by GWO for predicting. (a) Crack width (CW), (b) volumetric shrinkage (VS), and (c) linear shrinkage (LS).
Figure 14: The values of R-squared for MFO models. (a) Crack width (CW), (b) volumetric shrinkage (VS), and (c) linear shrinkage (LS).

Figure 15: Continued.
Figure 15: MSE calculated by MFO for predicting, (a) Crack width (CW), (b) volumetric shrinkage (VS), and (c) linear shrinkage (LS).

Figure 16: A schematic view of the attained ANN structure in this study.

Table 9: The optimal ANN parameters for outputs (CW, VS, and LS).

| Parameter                                      | Common value  |
|------------------------------------------------|---------------|
| Number of hidden layers                        | 2             |
| Number of neurons in hidden layers              | 11–7          |
| Type of activation function                    | Log – sig     |
| Type of learning algorithm                     | Levenberg–Marquardt |
| Number of train parameter epochs                | 500           |

Table 10: Performance indicator values for building ANN models for outputs (CW, VS, and LS).

| Model | Train | Test |
|-------|-------|------|
|       | $R^2$ | VAF  | RMSE | MAE  | VAF  | RMSE | MAE  |
| CW    | 0.999 | 99.982 | 0.017 | 0.012 | 0.961 | 94.868 | 0.354 | 0.164 |
| VS    | 0.999 | 99.988 | 0.020 | 0.011 | 0.999 | 99.860 | 0.070 | 0.032 |
| LS    | 0.999 | 99.997 | 0.003 | 0.002 | 0.999 | 99.468 | 0.038 | 0.014 |
Figure 17: The values of R-squared for ANN models. (a) Crack width (CW), (b) volumetric shrinkage (VS), and (c) linear shrinkage (LS).

Table 11: The best predicted values of $R^2$, VAF, RMSE, and MAE for predict CW, vs, and LS.

| Model | $R^2$ | VAF  | RMSE | MAE  | $R^2$ | VAF  | RMSE | MAE  |
|-------|-------|------|------|------|-------|------|------|------|
| LMR   | CW    | 0.854| 85.386| 0.558| 0.450 | 0.884| 87.686| 0.603| 0.495|
|       | VS    | 0.994| 99.986| 0.124| 0.124 | 0.999| 99.899| 0.126| 0.123|
|       | LS    | 0.988| 98.739| 0.596| 0.982 | 98.108| 0.606| 0.601|
|       | CW    | 0.927| 92.708| 0.349| 0.235 | 0.916 | 91.512| 0.434| 0.266|
| GWO   | VS    | 0.999| 99.972| 0.029| 0.021 | 0.999 | 99.866| 0.067| 0.034|
|       | LS    | 0.985| 98.543| 0.062| 0.033 | 0.985 | 98.543| 0.062| 0.033|
|       | CW    | 0.926| 92.556| 0.352| 0.262 | 0.902 | 89.876| 0.477| 0.341|
| MFO   | VS    | 0.994| 99.432| 0.131| 0.106 | 0.989 | 98.981| 0.186| 0.133|
|       | LS    | 0.989| 98.864| 0.053| 0.032 | 0.982 | 98.200| 0.069| 0.041|
|       | CW    | 0.999| 99.982| 0.017| 0.012 | 0.961 | 94.868| 0.354| 0.164|
| ANN   | VS    | 0.999| 99.988| 0.020| 0.011 | 0.999 | 99.860| 0.070| 0.032|
|       | LS    | 0.999| 99.997| 0.003| 0.002 | 0.999 | 99.468| 0.038| 0.014|
correlation of the collected data, and if the best models are based on case indices. Consider that ANN had the best performance in predicting all outputs, and then it can be seen that GWO, MFO, and LMR had the best performance in predicting CW, VS, and LS, respectively. This implies that ANN has the more flexibility to be used in predicting the parameters of the desiccation process with high performance indices. However, the three AI techniques have shown the potential to train and predict engineering problems from multiple data points with high performance index of above 90%.

3.7. Sensitivity Analysis. Sensitivity analysis was performed to identify the relative impact of each parameter on output in the model using the cosine domain method [40]. To apply this method, all of the data pairs should be utilized to build a data array $X$ as follows [3, 4, 41, 42]:

$$X = \{x_1, x_2, x_3, \ldots, x_i, \ldots, x_n\}. \quad (12)$$

Each of the elements, $x_i$, in the data array $X$ is a vector of lengths of $m$; that is,

$$X = \{x_{11}, x_{12}, x_{13}, \ldots, x_{im}\}. \quad (13)$$

The strength of the relation between the dataset, $x_i$ and $x_j$, is presented as follows:

$$r_{ij} = \frac{\sum_{k=1}^{m} x_{ik} x_{jk}}{\sqrt{\sum_{k=1}^{m} x_{ik}^2 \sum_{k=1}^{m} x_{jk}^2}} \quad (14)$$

According to Figure 18, which shows the strengths of the relationships (ridge values) between the inputs and outputs of the model, it is concluded that drying (T), diameter (D), volume (V), height (H), Wt of spec. (W), and HSDA (P) had the highest impact on CW, respectively, while for VS and LS, drying (T), diameter (D), height (H), volume (V), Wt of spec. (W), and HSDA (P) had the most impact, respectively.

4. Conclusions

Artificial neural network (ANN), gray-wolf, and moth-flame optimization (GWO and MFO) techniques were used to predict the effect of activated sawdust ash (ASDA) on the desiccation properties; crack width (CW), linear shrinkage (LS), and volumetric shrinkage (VS) of black cotton soil utilized as a subgrade material. From the foregoing, the following can be concluded.

(i) There was appreciable improvement in the shrinkage and crack parameters over the 30-day drying period due to the addition of waste-based ASDA.

(ii) The intelligent model results showed that the three techniques successfully predicted the CW, VS, and LS with a performance accuracy of 96.1%, 99.9%, and 99.9%, respectively, for the ANN; 90.2%, 98.9%, and 98.2%, respectively, for the MFO; 91.6%, 99.9%, and 98.5%, respectively for the GWO, but ANN produce the minimal error in performance out-performing the other techniques.

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**Figure 18:** Sensitivity analysis to determine the impact of each data on the output for (a) crack width (CW), (b) volumetric shrinkage (VS), and (c) linear shrinkage (LS).
(iii) The sensitivity analysis showed that drying period (T) was the most influential of the parameters studied in this model [43,44].

Data Availability

The data supporting the results of this research has been reported in the paper.

Conflicts of Interest

The authors declare that they have no conflicts of interest.

Supplementary Materials

The supplementary file is the tabulation of the multiple data collected from multiple experiments on drying days, weight, height, diameter, volume, crack width, volumetric shrinkage, and linear shrinkage of the hybrid sawdust ash (HSDA) treated black cotton soil (BCS). For a period of 30 days, these parameters were observed and recorded under laboratory conditions. The soil was treated with 3, 6, 9, and 12% by weight of soil of HSDA and specimens were prepared and placed in the oven for drying. (Supplementary Materials)

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