Comparative Studies of Self-organizing Algorithms for Forecasting Economic Parameters

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Abstract: This manuscript presents the economic research results based on their input-output characteristics and functional description with inductive modeling methods and tools. There are a wide plethora of methods to be used for solving this type of problem, including various neural network models, linear and nonlinear regressions, reference vectors’ methods, fuzzy models, etc. The main disadvantage of these methods is that the obtained models cannot always interpret and obtain a model of optimal complexity. Unlike the mentioned methods and tools, the group method of data handling (GMDH) allows building models directly from a data sample without the attraction of additional a priori information. This algorithm admits finding internal dependencies in the data and determining optimal model complexity. There is a broad range of iterative GMDH algorithms that have been developed and studied. Oversampling algorithms are applicable for solving the structural identification problems for a limited number of arguments. Iteration algorithms are suitable for solving tasks with many arguments, but they do not guarantee proper structure development. Multi-row GMDH iteration algorithms are the most popular ones. However, they have several sufficient defects, such as informative argument loss or non-informative argument inclusion, as well as a polynomial degree of exponential growth. In this context, the applicability of the GMDH-based iterative and combined architectures for solving the model’s interrelation problems between a volume of capital investments and GDP by activity types in the transport branch is considered. The determination coefficient is utilized for the estimation of the obtained models based on a complicated evaluation procedure. The Kolmogorov-Smirnov criterion estimates the model’s adequacy. The F-criterion Fisher assesses the significance of polynomial models. The demonstrated results proved that the combined iterative and combinatorial algorithms turned out to be the most effective solution for all evaluation criteria.

Index Terms: Group Method of Data Handling; Iterative Algorithm; Gross Domestic Product; Investment; Model Adequacy.
1. Introduction

Successful implementation of the investment policy will contribute to implementing one of the leading countries’ economic tasks to increase the number of primary domestic investment resources sources. This will create the necessary prerequisites for the production growth and expanded reproduction of GDP to increase the population’s well-being.

Therefore, it would be advisable to determine the informative investment indicators that have the most significant impact on the dynamics of Ukraine’s GDP. It is necessary to develop a model of the relationship between capital investment and GDP.

In [1], the author defined investment as “the current increase in capital property values as a result of production activities during a given period,” or as a share of income for a given period that was not used for consumption. The investment is said to be the material basis for the economy’s structuring. Solving the problem of investment will mean the beginning of not only the economy’s restructuring but also its stabilization and subsequent growth [2].

The term “investment” has several meanings. First, it means the purchase of shares, bonds with the expectation of specific financial results. Secondly, real assets like machinery, equipment necessary for the production and sale of any goods seem to be a great option. In the broadest sense, investments provide the mechanism necessary to finance the growth and development of the country’s economy, region, industry, or enterprise.

Successful implementation of the investment policy will contribute to implementing one of the main tasks of the country’s economy to increase the number of primary sources of domestic investment resources. This will create the necessary prerequisites for the production growth and expanded reproduction of GDP to increase the population’s well-being.

Complex economic processes are characterized by input and output variables and parameters that determine the object's internal state and depend on numerous random factors. It is known that economic processes are characterized by instability and instability. At the same time, well-known models in practice are often unsuitable for forecasting. In such situations, for the analysis, modeling, and forecasting of these processes, it is advisable to apply direct construction methods from observational results (statistics). The purpose of such methods is the identification of implicit causal relationships and patterns hidden in the data and the construction of mathematical models in explicit form. Therefore, obtaining an adequate mathematical description of such processes is a complex research project.

Static methods are used to describe stochastic processes, which allow us to extract the necessary results with incomplete information about the economic process’s mechanisms. One of the most acceptable methods for solving complex tasks related to modeling investment processes is the group method of data handling (GMDH) [3, 4].

The GMDH algorithms are widely used for solving identification problems of high order nonlinear dependencies between input and output variables. Even though these algorithms can cope with high-dimensional data and successfully cope with forecasting and modeling complex nonlinear processes, the questions of selecting a subset of variables necessary for a significant dimensionality reduction are still unclear. At present, there are a plethora of methods for the implementation of the self-organization idea [5, 6]. However, there is a problem in choosing the most effective models [7]. Therefore, a comparative study is carried out by algorithms of the GMDH iterative combinatorial type to identify the hidden dependencies between different types of capital investments in the transport industry and GDP.

In this study, we did not limit the study to evaluating the accuracy of the obtained models but assessed their adequacy and significance.

The novelty of this research has to do with:

- A new extended method based on the comparative analysis of the GMDH iteration algorithms has been developed;
- A methodology for estimating GDP from the volume of investments in the transport sector has been proposed.

The work aims to develop and research models of the relationship between the volume of capital investments and GDP by type of activity in the transport industry.

This article is arranged as follows. Section II gives a formal statement of the problem. Section III presents a detailed analysis of the work based on models of complex systems using inductive simulation tools to describe the system's input and output characteristics. Section IV describes methods of applying linear and nonlinear inductive GMDH models, as well as methods of assessing their quality. Section V presents the obtained experimental results. Finally, concluding remarks are given in Section VI.

2. Problem Statement

Such a statement is to find the extremum of some criterion \( CR \) on the set of different models \( 3 \):

\[
 f^* = \arg \min_{f \in 3} CR(f). \tag{1}
\]
Since (1) is not completed by the formulation of the problem, it needs to be further identified, in particular: to ask a priori expert or expert information about the kind, character, and volume of the initial information to be known from the analysis of the experiment; to specify a class of essential functions from which the set must be formed $\mathcal{A}$; to determine how to generate models $f$; to set the method of estimating parameters; to set the model comparison criterion $CR(f)$ and specify a method for minimizing it. Specify this statement, assuming that the given sample $W = [X, y]$ contains observation $n$ points that form the matrix $X = \{x_{ij}, i = 1,..., n; j = 1,..., m\}$ and the vector $y = (y_1, y_2, ... y_n)^T$, for which $n \geq m$.

In general, the process of constructing models according to experimental data (1) includes, in particular, the following main stages:

- Specifying a sample of experimental data, a priori, and expert information, and dividing the data table into at least two non-disjoint subsets;
- Definition of a class of essential functions;
- Generation different patterns of models in the selected class;
- Evaluation of the parameters of the generated structures and the formation of the set $\mathcal{A}$;
- Minimization of the given criterion $CR(f)$ and choice of the optimal model $f^*$;
- Checking the adequacy of the optimum model obtained;
- The decision to complete the simulation process.

3. Related Works

In the problems of constructing models of complex systems in the conditions of incomplete information, methods and means of inductive modeling are actively used, primarily intended for the functional description of the input-output characteristics of the systems.

The first part of the preliminary literature review was described in the Introduction. Furthermore, some more specific issues are dwelled on in this section.

The scientific direction is called "inductive modeling of complex processes and systems," formed by Alexei Ivakhnenko [8].

The author called this new direction differently: first, "heuristic self-organization" [9], later "self-organization of models based on experimental data" [10], then "inductive self-organization of models of complex systems" [11].

Finally, the various methods of modeling that can be classified as inductive are highlighted by the group method of data handling (GMDH), allowing to build models directly on data sampling without attracting additional a priori information [12, 13].

GMDH is successfully used in data analysis and identification of patterns, modeling, forecasting [14], structural identification, clustering, classification, and pattern recognition [15, 16].

It allows you to automatically find interdependencies and patterns implicitly reflected in the data, and present them in an explicit form of mathematical models of optimal complexity.

As of today, many varieties of algorithms GMDH of robotic [17] and iterative [3] types have been developed and investigated. Reordering algorithms are practical as a means of structural identification, but only for a limited number of arguments since they are based on a full or directed enumeration of all possible variants of model structures [18].

Iterative algorithms work with a sufficiently large number of arguments. However, the specificity of their architecture does not guarantee the construction of a proper structure model, since they are based on incomplete inductive procedures for hierarchically complicating models. For a long time, these two classes of algorithms developed independently, without a detailed study of the possibility of combining their strengths while eliminating shortcomings [19].

4. Applied Methods

The following macroeconomic indicators for the period from 2012 (1st quarter) to 2017 (4th quarter) - 24 points were taken as experimental data for calculating the dependence between the Ukraine's GDP growth and the volume of investment in the transport industry (http://www.ukrstat.gov.ua/).

In Table I, there are numerical values used to build models of statistic data on capital includity and calculation of an including product on types of activities "transport, warning, leading and courier activities".

- $x_1$ is the volume of investments in land and pipeline;
- $x_2$ is the volume of investment in water transport;
- $x_3$ is the volume of investment in air transport;
- $x_4$ is the volume of investments in warehousing and auxiliary activities in the field of transport;
- $x_5$ is the volume of investments in postal and courier activities.
In general, the data set is divided into two parts: 16 measurements are training sample A, eight measurements are a test sample B.

It is necessary to establish a model of the relationship between the volume of capital investments and GDP by type of activity "Transport, warehousing, postal and courier activities."

In this paper, a model simulation class is considered for a statistical sample containing information about \( n \) observations for \( m \) input variables \( X \) \([n \times m]\) and one output variable \( y \) \([n \times 1]\).

It is necessary to find a model of the input-output dependence in the conditions of incompleteness and uncertainty of information on the structure of this dependence.

From the available positions, the task of identification is to form a sample of experimental data for a particular set \( \mathfrak{T} \) of models of the different structure of the species [20]:

\[
\hat{y}_f = f \left( X, \hat{\theta}_f \right)
\]  

(2)

According to [20], in the formation \( w = \langle X : y \rangle \) of a sample \( \mathfrak{T} \) of a plurality of different structures models of the species \( \hat{y}_f = f(X, \theta_f) \) and the search for an optimal model for a minimum of a given criterion according to the data of a sample \( CR(\cdot) \):

\[
f^* = \arg \min_{f \in \mathfrak{T}} CR(y, f(X, \theta_f)),
\]

where estimating the parameters \( \theta_f \) for each model \( f \in \mathfrak{T} \) is the solution to another problem of the form:

\[
\hat{\theta}_f = \arg \min_{f \in \mathfrak{T}_f} Q(y, X, \theta_f)
\]

(4)

where \( Q(\cdot) \neq CR(\cdot) \) – the quality criterion for solving the problem of parametric identification of a partial model that has the complexity \( S_f \) generated in the task of structural identification (3).

For example, the external criteria \( CR(\cdot) \) for regularity or unbounding, based on a sample split, can be used as a criterion in the GMDH.

The criterion of regularity (expresses the model error in different parts of the sample). Since the second principle of inductive modeling of complex systems on the principles of GMDH is the principle of external complement, which requires breakdown of the table of output data into the training (A) and control (test - B) part, then as a criterion Regularity, and all the others that will be mentioned here, still have the application of "external," which emphasizes this principle.

The regularity criterion is used to solve pattern recognition tasks, identification, and prognosis, and in one of the most straightforward variants, it has the form:

\[
\Lambda \left( \mathfrak{B} \right) = \left( \sum_{q \in A} (q_f - \hat{q}_w)^2 \right) / \left( \sum_{q \in \mathfrak{B}} \hat{q}_w^2 \right) \to \min
\]

(5)

where \( q_f \) — actual (tabular) data; \( \hat{q}_w \) — output of the model; \( N = N_A + N_B \) — the set of points of the output data is divided into two parts: \( N_A \) and \( N_B \).

The regularity criterion (5) was also used in the form of the correlation coefficient between the variables \( q_f \) and \( \hat{q}_w \) inside the interval of data \( B \) or the correlation index (for nonlinear models).

To simulate the dependence of GDP growth in Ukraine (UAH Million) on the volume of investments, iterative algorithms were used, including three linear algorithms and six with a quadratic function, including combined algorithms for constructing models:

Linear:
1) multi-row iterative (lin m);
2) relaxation (lin r);
3) combined iterative (lin c);
   With quadratic function:
4) multi-row iterative with quadratic function (sq m);
5) a relaxation quadratic function (sq r);
6) a relaxation-combinatorial quadratic function (sq c);
7) multi-row iterative-combined (sq combi m);
8) relaxation iterative-combined (sq combi r);
9) combined iterative-combinatorial (sq combi m).

A. Multi order Iterative Algorithm of GMDH

In the classical multi-row algorithm of GMDH, the problem of constructing an optimal model is solved inductively: the model of a gradually complicated structure is constructed, and the process of complication has the character of iterations when the best preliminary results are used in the next series (iterations).

The complication is the only rule that allows you to build an arbitrarily complex model from a large number of variables (arguments) that characterize the object of modeling [18].

Consider the more complex operations performed on the 1st and arbitrary (r + 1)-th ranks.

Table 1. Statistical Data of Capital Investments and Gross Domestic Product by Type of Activity "Transport, Warehousing, Postal and Courier Activity"

| Years         | Ground and pipeline transport | Water transport | Air transport | Warehousing and auxiliary transport activities | Postal and courier activities | GDP, mln. UAH |
|--------------|-------------------------------|----------------|-------------|-----------------------------------------------|-------------------------------|---------------|
|              | Capital investment, mln. UAH |                |             |                                               |                               |               |
|              | X1                            | X2             | X3          | X4                                            | X5                            | Y             |
| 1st quarter 2012 | 1992,1                        | 35,7           | 275,3       | 2820,1                                        | 20,4                         | 292894        |
| 2nd quarter 2012 | 4378,5                        | 26,8           | 176,0       | 3642,6                                        | 35,4                         | 354872        |
| 3rd quarter 2012 | 2651,8                        | 41,7           | 133,5       | 3581,9                                        | 168                          | 389213        |
| 4th quarter 2012 | 3691,8                        | 28,4           | 195,2       | 4140,5                                        | 172,4                        | 381289        |
| 1st quarter 2013 | 587,8                         | 6,3            | 98,6        | 1779,2                                        | 5,0                          | 307353        |
| 2nd quarter 2013 | 1189,4                        | 37,3           | 137,6       | 2042,0                                        | 5,1                          | 354814        |
| 3rd quarter 2013 | 1440,2                        | 31,8           | 131,6       | 3039,0                                        | 8,2                          | 398000        |
| 4th quarter 2013 | 1650,3                        | 21,4           | 155,3       | 3929,4                                        | 202,1                        | 408631        |
| 1st quarter 2014 | 590,3                         | 29,3           | 73,3        | 1876,8                                        | 3,8                          | 316905        |
| 2nd quarter 2014 | 1140,6                        | 41,0           | 79,2        | 2230,4                                        | 4,1                          | 382391        |
| 3rd quarter 2014 | 652,3                         | 89,0           | 71,4        | 1820,4                                        | 9,1                          | 440476        |
| 4th quarter 2014 | 1072,6                        | 48,8           | 96,2        | 3921,9                                        | 105,5                        | 447143        |
| 1st quarter 2015 | 1805,6                        | 23,1           | 116,3       | 904,4                                         | 4,9                          | 375991        |
| 2nd quarter 2015 | 874,6                         | 96,2           | 193,7       | 1935,6                                        | 2,8                          | 456715        |
| 3rd quarter 2015 | 2386,9                        | 111,6          | 125,6       | 2083,2                                        | 5,3                          | 566997        |
| 4th quarter 2015 | 2150,9                        | 102,9          | 223,1       | 3058,7                                        | 72,6                         | 588441        |
| 1st quarter 2016 | 1952,2                        | 36,6           | 99,2        | 1439,6                                        | 13,3                         | 455299        |
| 2nd quarter 2016 | 2256,5                        | 38,0           | 177,7       | 2114,6                                        | 22,5                         | 535701        |
| 3rd quarter 2016 | 3365,5                        | 53,3           | 218,4       | 2646,5                                        | 18,7                         | 671456        |
| 4th quarter 2016 | 7383,0                        | 106,2          | 202,3       | 2527,1                                        | 66,5                         | 722912        |
| 1st quarter 2017 | 3693,0                        | 50,8           | 210,2       | 1454,0                                        | 6,6                          | 591008        |
| 2nd quarter 2017 | 4181,9                        | 55,4           | 260,4       | 1979,0                                        | 51,8                         | 664760        |
| 3rd quarter 2017 | 4627,7                        | 56,9           | 372,2       | 2852,1                                        | 53,7                         | 831380        |
| 4th quarter 2017 | 9455,6                        | 74,6           | 340,4       | 5640,6                                        | 285,3                        | 894022        |

The first iteration (first row). From the set of inputs \( X = \{x_1, x_2, \ldots, x_n\} \), pairs of arguments are chosen, and partial views of the form are formed:

\[
\begin{align*}
z &= f(u, v) = a_0 + a_1u + a_2v; \\
\bar{z} &= f(\bar{u}, \bar{v}) = a_0 + a_1\bar{u} + a_2\bar{v}; \\
\tilde{z} &= a_0 + a_1u + a_2v + a_3uv + a_4u^2 + a_5v^2. 
\end{align*}
\]  

That is, \( y_1^l = f(x_1, x_2), \ l = 1, 2, 3, \ldots, C^m_n \), and according to the MNA, for each description, according to the data of the training sample, estimates of unknown parameters (coefficients) \( \tilde{a}_0, \tilde{a}_1, \tilde{a}_2, \ldots \) are presented. By the chosen criterion, on the test sample, \( F \) chooses the best models \( y_1^k, \ k = 1, \bar{F} \); that is, they implement the selection procedure, where \( F \) is...
called the freedom of choice. The outputs of these models are arguments-inputs for constructing models of the next series. The following is the minimum $CR_{min}^1$ among all $F$ values of the criterion in the first row.

An arbitrary $(r + 1)$ iteration (series $r + 1$): From the argument vectors $y^r_j$, $k = 1, F$, the previous $r$-th row, all possible partial description of the form (6) is formed, that is:

$$y^{r+1}_i = f(y^r_j, y^r_j), \quad l = 1, 2, \ldots, C^2_F, \quad i, j = 1, F$$ (7)

Furthermore, according to the MNA, $A$ parameters are evaluated. According to the selection criterion, $F$ is selected as the best model $y^r_j, k = 1, F$, among which is $CR_{min}^{r+1}$ the condition $CR_{min}^{r+1} \geq CR_{min}^r$ that the iteration process stops; otherwise the transition to the next series is checked. In the case of stopping the process, the model corresponding to the value $CR_{min}^r$ in the previous $r$-series is accepted as the optimal one.

C. The Relaxation Iterative Algorithm (RIA)

The name of the relaxation iterative algorithm (RIA) corresponds to the analogy with optimization algorithms. In this algorithm, in each row, the intermediate arguments are combined in pairs with the original [21], which prevents loss of informative arguments, with such possible variants of linear, bilinear, or partial quadratic descriptions:

$$y^r_j = a_0 + a_1 y^{r-1}_j + a_2 x_j$$
$$y^r_j = a_0 + a_1 y^{r-1}_j + a_2 x_j + a_3 y^{r-1}_j x_j$$
$$y^r_j = a_0 + a_1 y^{r-1}_j + a_2 x_j + a_3 (y^{r-1}_j)^2 + a_4 y^{r-1}_j x_j + a_5 (x_j)^2$$ (8)

Description of the algorithm. The first row is executed as in the classic multi-row algorithm.

An arbitrary $(r + 1)$ - this iteration (row $r + 1$). From the argument vectors $y^r_j, k = 1, F$, the previous $r$-series, all possible partial description of the form (8) is formed, i.e.:

$$y^{r+1}_i = f(y^r_j, x_j), \quad l = 1, 2, \ldots, C^2_F, \quad i, j = 1, F$$ (9)

Moreover, for the MNA on $A$, there are parameter estimates. Then, according to the selection criterion, $F$ selected the best models $y^{r+1}_j, k = 1, F$, and is located $CR_{min}^{r+1}$ and verifies the condition $CR_{min}^{r+1} \geq CR_{min}^r$ in which the iterative process stops, otherwise the transition to the next row. In the case of a stop, an optimal model is adopted, which corresponds to the value $CR_{min}^r$ in the previous $r$-series.

In this algorithm, it is also possible to use different partial descriptions on different rows to reduce the complexity of models, for example, using the second-order polynomial in the first row and only the linear form for the following series.

D. Combined Iterative Algorithm

This algorithm from the previous is different in that each pair of pairs are formed only from intermediate arguments and from intermediate and initial [22].

Description of the algorithm. The first row is executed as in the classic multi-row algorithm.

An arbitrary $(r + 1)$ -this iteration (row $r + 1$). From vector arguments $y^r_j, k = 1, F$, the previous $r$-th row generates all possible partial descriptions of the form (1) or (8), i.e.:

$$y^{r+1}_i = f(y^r_j, y^r_j) \lor f(y^r_j, x_j),$$
$$l = 1, 2, \ldots, C^2_F, \quad i, j = 1, F$$ (10)

Moreover, for the MNA on $A$, there are parameter estimates. Then, according to the selection criterion, $F$ selected the best models $y^{r+1}_j, k = 1, F$, and is located $CR_{min}^{r+1}$ and verifies the condition $CR_{min}^{r+1} \geq CR_{min}^r$ in which the
iterative process stops, otherwise the transition to the next row. In the case of a stop, an optimal model is adopted, which corresponds to the previous \( r \)-series's value \( C_{\text{min}}^R \).

E. Multi-Row Iterative-Combinatorial Algorithm

The combinatorial optimization of partial descriptions, that is, the application of the idea of active neurons - linear, bilinear, or nonlinear - can be applied in each of the varieties of iterative algorithms [23].

Consider the more complex operations performed on an arbitrary \((r + 1)\)-th series (including on the first one).

An arbitrary \((r + 1)\)-th iteration (row \(r + 1\)). The previous \(r\)-th row (or input arguments, if it is the first row), all possible partial descriptions \((1)\) are formed from vector arguments. Combinatorial optimization consists in the fact that on each row models are considered, for example, such a kind (for a partial linear description):

\[
y_i^{(r+1)} = f_{opt}(y_i^r, y_j^r) = a_0 + d_1 y_i^{r-1} + d_2 y_j^{r-1}
\]

where \(d_k, k = 1, 2, 3\) are elements of the binary structural vector \(d\) that accept values 1 or 0 (inclusion or not the inclusion of the corresponding argument):

\[
d_k = \{0, 1\}, \quad d_{\text{opt}} = \arg \min_{i=1,q} CR_i, \quad q = 2^r - 1, \quad f_{opt}(u, v) = f(u, v, d_{\text{opt}}).
\]

The layout of the survey then has the form:

\[
\begin{align*}
100 & \rightarrow f_1 = a_0 & CR_1 \\
010 & \rightarrow f_2 = a_1 y_i^{r-1} \quad CR_2 \\
001 & \rightarrow f_3 = \quad a_1 y_j^{r-1} \quad CR_3 \\
110 & \rightarrow f_4 = a_0 + a_1 y_i^{r-1} \quad CR_4 \Rightarrow f_{\text{opt}} \\
101 & \rightarrow f_5 = a_0 + a_1 y_j^{r-1} \quad CR_5 \\
011 & \rightarrow f_6 = a_0 + a_1 y_i^{r-1} + a_2 y_j^{r-1} \quad CR_6 \\
111 & \rightarrow f_7 = a_0 + a_1 y_j^{r-1} + a_2 y_i^{r-1} \quad CR_7
\end{align*}
\]

At the same time, the best option for the CR criterion minimum is selected, i.e., the complexity of the partial model is optimized:

\[
d_{\text{opt}} = \arg \min_{i=1,q} CR_i, \quad q = 2^r - 1, \quad f_{\text{opt}}(u, v) = f(u, v, d_{\text{opt}})
\]

Then, according to the selection criterion, \(F\) selected the best models \(y_k^{(r+1)}, k = 1, F\) and is located \(C_{\text{min}}^{R*r+1}\) and verifies the condition \(C_{\text{min}}^{R*r+1}\) in which the iterative process stops, otherwise the transition to the next row. In the case of a stop, an optimal model is adopted, which corresponds to the value \(C_{\text{min}}^{R*r}\) in the previous \(r\)-series.

F. Relaxation Iterative-Combinatorial Algorithm [24]

By adding in the multi-row iterative-combinatorial algorithm, the possibility to combine intermediate arguments in each row in pairs with the initial ones receive a relaxation iterative-combinatorial algorithm.

An arbitrary \((r + 1)\)-th iteration (row \(r + 1\)). From vector arguments \(\chi_k, k = 1, F\). The previous \(r\)-th row (or input arguments, if it is the first row), all possible partial descriptions \((1)\) are formed. Combinatorial optimization consists in the fact that on each row models are considered, for example, such a kind (for a partial linear description):

\[
y_i^{(r+1)} = f_{\text{opt}}(y_i^r, x_j^r) = a_0 + d_1 y_i^{r-1} + d_2 y_j^{r-1} + d_3 x_j^{r-1}
\]

where \(d_k, k = 1, 2, 3\) are elements of binary structural vector \(d\), which accept values 1 or 0 (inclusion or not the inclusion of the corresponding argument):
Then, according to the selection criterion, F is selected as the best model of the series.

G. Combined iterative-combinatorial algorithm (CICA)

CICA or generalized iterative algorithm (GIA). The combinatorial optimization of partial model structures in the combined algorithm gives the algorithm the full name of the "combined iterative-combinatorial algorithm" of CICA. His further generalization, which takes into account both CICA and all its partial cases, as well as various variants of operating modes implemented through the user interface, are called "Generalized iteration algorithm" or GIA GMDH [13, 19, 25].

Formally, in the general case, for a series r, it is possible to define the GIA of the GMDH as follows [26]:

1) the input matrix is \( X_{r,t} = (y'_1, ..., y'_q, x_1, ..., x_n) \);
2) the transition type operators are used:
\[
y^{i+1}_l = f(y^{j+1}_l, y^{j+1}_i), \quad l = 1, 2, K, C_{j+1}, \quad i, j = 1, F,
\]
\[
y^{i+1}_l = f(y^{j+1}_l, x_i), \quad l = 1, 2, K, F, i = 1, F, \quad j = 1, m
\]

(14)

with a linear, bilinear, or partial quadratic description (1):

for each description is the optimal structure, n-d, for the linear form:
\[
f(u, v) = a_0 d_1 + a_1 d_2 u + a_2 d_3 v
\]

(15)

where \( d_k, k = 1, 2, 3 \) are elements of the binary structural vector \( d \) that accept values 1 or 0 (inclusion or non-inclusion of the corresponding argument):
\[
d_k = \{0, 1\}, \quad d_{opt} = \arg\min_{i\in q} CR_i, \quad q = 2^q - 1, \quad f_{opt}(u, v) = f(u, v, d_{opt}).
\]

4) the algorithm stops when the condition \( CR_{max}^{r+1} \geq CR_{max}^r \) is fulfilled, and the optimal model corresponds to the value \( CR_{max}^r \) on the \( r \)-th row.

H. The Accuracy of the Models

The accuracy of the models obtained was based on the formula of the determination coefficient (\( R^2 \) - statistics):
\[
R^2 = \frac{\sum_{i=1}^{n} \left( y_i - \hat{y}_i \right)^2}{\sum_{i=1}^{n} \left( y_i - \bar{y} \right)^2} \times 100\%,
\]

(16)

where \( \bar{y} \) is an average value and \( \hat{y}_i \) is an output of the model.

The determination coefficient characterizes the fraction of the variance of the resultant variable \( Y \), an explanation of the polynomial regression, in the overall variance of the resultant variable \( Y \). Accordingly, the magnitude \( 1 - R^2 \) characterizes the fraction of the variance of the variable \( Y \) caused by the influence of other factors not taken into account in the model.

I. Adequacy of the Obtained Models

The criterion by Kolmogorov-Smirnov is intended to determine that the sample has a corresponding distribution; in our case, is expected. For example, the hypothesis is checked that the sample has a normal distribution. The small value of probability means the rejection of the hypothesis of normality. For a sample with a normal distribution, the probability value tends to be unity.
Let $X_\alpha$ be a sample of independent equally distributed random variables, $F_\alpha(x)$ is an empirical distribution function, $F(x)$ stands for a specific "true" distribution function with known parameters. The statistics of the criterion are determined by the following expression:

$$D_\alpha = \sup_x \left| F_\alpha(x) - F(x) \right|$$ (17)

We denote by the $H_\alpha$ hypothesis that the sample is subject to distribution $F(x) \in C(X)$. Then Kolmogorov's theorem is validated by the hypothesis:

$$\forall t > 0: \lim_{n \to \infty} P(\sqrt{n} \| D_\alpha \| \leq t) = K(t) = \sum_{j=-\infty}^{+\infty} (-1)^j e^{-2j^2t^2}$$ (18)

Hypothesis $H_0$ rejected if statistics $\sqrt{n} \| D_\alpha \|$ exceeds quantile distribution $K_\alpha$, the given level of significance $\alpha$ and is accepted otherwise. In Kolmogorov's criterion, it is expedient to use statistics with the correction of Bolshev [27]:

$$\sqrt{n} \| D_\alpha \| + 1 / (6 \sqrt{n})$$. The distribution of these statistics with fairness is verified by the hypothesis quickly converges to the distribution of Kolmogorov, and depending on the size of the sample can be neglected. In the Kolmogorov-Smirnov test for one sample, hypotheses are tested:

- Hypothesis 0 (zero): Deviation from a normal distribution is significant
- Hypothesis 1 (alternative): The values of the variable are well suited to the normal distribution.

The probability of an error in which it is permissible to reject the null hypothesis and accept an alternative hypothesis is defined as a value that is in the range from 0 to 1.

Usually, the probability is denoted by the letter $p$: $0 < p < 0$. There is a commonly used terminology that relates to confidence intervals of probability. Expressions with a probability of error $p \leq 0.05$ are called meaningful; statements with a probability of error $p \leq 0.01$ - very significant, and statements with the probability of errors $p < 0.001$ - the most significant. A deviation from the normal distribution is considered significant at the value of $p < 0.05$; In this case, nonparametric tests should be used for the respective variables. In the considered example (the value of $p = 0.467$), that is, the probability of error is not significant, so the value of the variable is good enough to fit into the normal distribution.

A deviation from the normal distribution is considered significant at the value of $p < 0.05$; In this case, nonparametric tests should be used for the respective variables. In the example under consideration (the value of $p = 0.616$), the probability of error is not significant, so the variable's values are well suited to the normal distribution, and parametric tests can be used [28-30].

**I. The evaluation of the Obtained Models**

The evaluation of the significance of the entire regression equation as a whole is carried out using Fisher's F-criterion. Fisher's F-criterion consists of checking the null hypothesis about the statistical insignificance of the regression equation.

This is done by comparing the actual $F_{act}$, and the critical (tabular) values $F_{crit}$ of the F-criterion $F_{act}$ of Fisher. is determined from the ratio between the values of factor and residual variances, calculated for one degree of freedom:

$$F_{act} = \frac{\sum \frac{(\bar{y} - \bar{y})^2}{m}}{\sum \frac{(y - \bar{y})^2}{n - m - 1}} = \frac{R^2}{1 - R^2} \frac{n - m - 1}{m}$$ (19)

where $n$ is a number of units of the population; $m$ describes a number of parameters with variables $R^2$ (a coefficient of determination).
$F_{tabl}$ is the maximum possible value of the criterion under the influence of random factors with degrees of freedom $k_1 = m, k_2 = n - m - 1$ (for linear regression $m = 1$), and level of significance $\alpha$. The level of significance $\alpha$ is the probability of rejecting the correct hypothesis provided that it is true. Usually a value $\alpha$ equals 0.05 or 0.01. If $F_{tabl} < F_{fact}$, then, $H_0$, the random nature of the evaluated characteristics is rejected, and their statistical significance and reliability are recognized. If $F_{tabl} > F_{fact}$, then, the hypothesis does not deviate and recognizes the statistical insignificance, the unreliability of the regression equation.

The Kolmogorov-Smirnov criterion is acceptable to test the hypothesis, whether the random variable of some theoretical distribution law is obeyed if its parameters are assumed to be known (a simple hypothesis). The test can be carried out for any type of distribution.

The criterion is based on determining the maximum deviation of the accumulated frequency (empirical distribution function) from the predicted theoretical distribution function. The results are in the variation series. Find the upper and lower bounds of the corresponding deviation:

$$D^*_+ = \max \left\{ \frac{i}{n} - F(x_i) \right\},$$

at $1 \leq i \leq n$

$$D^-_* = \max \left\{ F(x_i) - \frac{x - 1}{n} \right\},$$

at $1 \leq i \leq n$

where $F(x_i)$ is the value of the theoretical distribution function. Choose the maximum outside the range of deviations:

$$D_* = \max \left\{ D^*_*, D^-_* \right\}.$$  

The criterion statistics can be calculated according to the formula:

$$\lambda = \frac{6nD_* + 1}{6\sqrt{n}}.$$  

The estimated value is compared with the table $\lambda_{tabl}$. Table values are previously known.

If $\lambda_{fact} \leq \lambda_{tabl}$, then the distribution is considered to be theoretical with the distribution function $F(x)$ with known parameters at the chosen level of significance $\alpha$.

5. Experiments and Results

The quality of the constructed model was calculated on the sub-sample B as the value of the regularity criterion $AR$ (1). The accuracy of the model was also tested on the sub-sample B as the value of the determination coefficient $R^2$ (Tables II and III).

For each object, the balance can be calculated $e_i = Y_i - \hat{Y}_i$, $i = 1, 2, K, n, i$, where $\hat{Y}_i$ is an estimated value. The balance is useful for studying the adequacy of the data model.

This means that the requirements for the residue independence for individual observations must be met; the variance should not depend on $X$. The results of assessing the adequacy of the models obtained using the Kolmogorov-Smirnov criteria are given in Tables IV.

The results of the evaluation of the significance of the whole equation of the obtained model using Fisher’s $F$-criterion are given in Table VI.
### Table 2. Simulation Results for Linear Dependence

| № | Algorithm's building models | AR Norm | $R^2$ | Model |
|---|---------------------------|---------|-------|-------|
| 1 | lin m | 0.098 | 0.558 | $y = 264387.04 + 2301.94 \times x_1 + 249.56 \times x_1^2 + 62.49 \times x_1^3 + 13.58 \times x_1^4$ |
| 2 | lin r | 0.109 | 0.561 | $y = 376393.94 + 64.00 \times x_1$ |
| 3 | lin c | 0.096 | 0.529 | $y = 284895.56 + 2287.49 \times x_1 + 346.53 \times x_1^2 - 83.39 \times x_1^3 - 10.18 \times x_1^4 + 16.85 x_1^5$ |

### Table 3. Simulation Results for Nonlinear Dependence

| № | Algorithm's building models | AR Norm | $R^2$ | Model |
|---|---------------------------|---------|-------|-------|
| 1 | sq m | 0.096 | 0.523 | $y = 466075.21 - 1728.12 \times x_1 - 116.49 \times x_1^2 + 19.28 \times x_1^3 + 0.02 \times x_1^4 + 0.8 \times x_1^5 \times x_1^6$ |
| 2 | sq r | 0.055 | 0.815 | $y = 132928.72 + 12.11 \times x_1 + 2243.14 \times x_1 + 3543.94 \times x_1^2 + 2.95 \times x_1^3 - 39.86 \times x_1^4 + 4.64 \times x_1^5 - 0.1 \times x_1^6 + 0.17 \times x_1^7 \times x_1^8$ |
| 3 | sq c | 0.034 | 0.809 | $y = 352822.33 - 10.27 \times x_1 + 0.003 \times x_1^2 + 4.93 \times x_1^3 + 0.004 \times x_1^4 \times x_1^5 \times x_1^6$ |
| 4 | sq combi m | 0.026 | 0.845 | $y = 354266.26 - 6.01 \times x_1 - 351.13 \times x_1 - 0.04 \times x_1^2 \times x_1^3 + x_1 + 0.03 \times x_1^2 \times 0.29 \times x_1^3 - 0.002 \times x_1^4 + 0.98 \times x_1^5 \times x_1^6 + 2.8 \times x_1^7 \times x_1^8$ |
| 5 | sq combi r | 0.026 | 0.871 | $y = 358151.48 + 1.38 \times x_1 - 0.01 \times x_1^2 + ? \times 0.01 \times x_1^2 \times x_1^3 \times x_1^4$ |
| 6 | sq combi c | 0.009 | 0.981 | $y = 292416 + 0.256097 \times x_1^x \times x_1 - 0.198123 \times x_1^x \times x_1 + 0.704721 \times x_1^x \times x_1^5$ |

### Table 4. Statistical Indicators of the Kolmogorov-Smirnov Criterion for Residues of Projections Obtained by the Polynomial Models

| Model | Lin m | Lin r | Lin c | Sq m | Sq r | sq c | Sq combi m | Sq combi r | Sq combi c |
|-------|-------|-------|-------|------|------|------|------------|------------|------------|
| Average value | 6.89 | -5.31 | 7.61 | 6.96 | 3.69 | 2.07 | 3.48 | 2.13 | -3.31 |
| Standard deviation | 1.17 | 1.62 | 1.28 | 1.95 | 8.9 | 1.28 | 6.66 | 6.01 | 7.23 |
| Extreme differences | 0.217 | 0.155 | 0.247 | 0.159 | 0.199 | 0.117 | 0.119 | 0.095 | 0.162 |
| Positive | 0.217 | 0.155 | 0.247 | 0.159 | 0.199 | 0.072 | 0.119 | 0.095 | 0.082 |
| Negative | -0.135 | -0.109 | -0.175 | -0.116 | -0.151 | -0.117 | -0.072 | -0.054 | -0.162 |
| Z Kolmogorov-Smirnov | 1.061 | 0.759 | 1.209 | 0.780 | 0.975 | 0.575 | 0.583 | 0.467 | 0.796 |
| Static value (2-sided) | 0.210 | 0.612 | 0.108 | 0.578 | 0.297 | 0.896 | 0.886 | 0.981 | 0.551 |
| Form of distribution | Normal | Normal | Normal | Normal | Normal | Normal | Normal | Normal | Normal |
Table 5. Statistical Parameters of the Fisher's Criterion for Residues of Predictions Obtained Using the Polynomial Models

| Model     | Fisher's F-criterion | Significance F | F critical |
|-----------|----------------------|----------------|------------|
| lim m     | 51.36                | 0.0000048      | 2.40       |
| lin r     | 55.5                 | 3.1000642      | 2.40       |
| lin c     | 17.39                | 0.000004811    | 2.40       |
| sq m      | 51.36                | 7.87787080     | 2.40       |
| sq r      | 102.79               | 0.025940648    | 2.40       |
| sq c      | 6.20                 | 0.0000113887   | 2.40       |
| sq combi m| 43.56               | 0.000011887    | 2.40       |
| sq combi r| 45.44               | 9.46225677     | 2.40       |
| sq combi c| 51.36                | 0.00000481143  | 2.40       |

A deviation from the normal distribution is considered significant at the value of $p < 0.05$. In this case, nonparametric tests should be used for the respective variables. Figures 1 and 2 show the results of the accuracy of the constructed model.

Fig. 1. An example of the graph.

Fig. 2. Simulation results of the combined iterative-combinatorial algorithm

6. Conclusion

Based on the results of a comparative analysis, the advantages and disadvantages of the existing inductive modeling algorithms have been presented; the efficiency of applying the iterative GMDH algorithms for solving model-building problems has been established.

A complex assessment of the obtained models was carried out so that the determination coefficient was used to assess the accuracy of the obtained models; at the same time, the Kolmogorov-Smirnov criterion was used to assess their adequacy. The significance of the polynomial models was estimated according to Fisher's F-test. The results have shown that the combined iterative-combinatorial algorithms are the most efficient in all the evaluation criteria.
A comprehensive technique for comparative analysis of the iterative GMDH algorithms using computational experiments has been developed for studying the influence of the algorithms’ pivot parameters on the performance indicators of the model’s development process.

Based on a series of the provided numerical experiments, the combined iterative-combinatorial algorithms have demonstrated a higher level of accuracy (98.1%) compared to the multi-row iterative-combined algorithms (84.5%) and the relational iterative-combined (87.1%). The performed results' evaluations through the Kolmogorov-Smirnov criteria and the F-Fisher test emphasize that the obtained polynomial models are quite adequate and have an optimal complexity level. It was proved that the indicators used for forecasting GDP have a compatible multiplier effect on GDP, which indicates a nonlinear relationship between the utilized investment indicators and GDP. The resulting models have optimal complexity and can be interpreted easily by experts.

The complicated method of the GMDH iterative algorithms’ efficiency numerical analysis allows a comprehensive study of the influence of the critical parameters of the compared algorithms on the leading indicators of the quality of the simulation results. The efficiency of using the methods of group accounting of arguments in forecasting GDP is shown.

It is proved that the indicators used in forecasting GDP have a compatible (synergistic) multiplicative effect on GDP, which indicates a nonlinear relationship between the used investment indicators and GDP.

In our further studies, we plan to use the developed methodology for solving problems in bioinformatics and immunoinformatics to determine the affinity of proteins and peptides, where the data are characterized by high dimensionality, nonlinearity, and noise.

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