Ultrafast-laser-absorption spectroscopy for single-shot, mid-infrared measurements of temperature, CO, and CH$_4$ in flames

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This manuscript describes the development of an ultrafast (i.e., femtosecond), mid-infrared, laser-absorption diagnostic and its initial application to measuring temperature, CO, and CH$_4$ in flames. The diagnostic employs a Ti:Sapphire oscillator emitting 55-fs pulses near 800 nm which were amplified and converted into the mid-infrared (mid-IR) through optical parametric amplification (OPA) at a repetition rate of 5 kHz. The pulses were directed through the test gas and into a high-speed mid-infrared spectrophotograph to image spectra across a $\approx 30$ nm bandwidth with a spectral resolution of $\approx 0.3$ nm. Gas properties were determined by least-squares fitting a spectroscopic model to measured single-shot absorbance spectra. The diagnostic was validated with measurements of temperature, CO, and CH$_4$ in a static-gas cell with an accuracy of 0.7% to 1.8% of known values. Single-shot, 5 kHz measurements of temperature and CO were acquired near 4.9 $\mu$m in a laser-ignited HMX (i.e., 1,3,5,7-tetranitro-1,3,5,7-tetrazoctane) flame and exhibited a 1–$\sigma$ precision of 0.4% at $\approx 2700$ K. Further, CH$_4$ and temperature measurements were acquired near 3.3 $\mu$m in a partially premixed CH$_4$-air flame produced by a Hencenk burner and exhibited a precision of 0.3% at $\approx 1000$ K.

\textit{laser-absorption spectroscopy, ultrafast spectroscopy, mid-wave infrared spectroscopy, broadband absorption spectroscopy}

Introduction

Laser-absorption spectroscopy (LAS) is a powerful technique for non-invasive, quantitative measurements of temperature and species concentrations in combustion environments (1). LAS diagnostics often employ narrowband, wavelength-tunable lasers (e.g., tunable diode lasers, quantum-cascade lasers) which are capable of measuring gas conditions via spectra measured over several cm$^{-1}$ at rates up to 1 MHz (1, 2). While highly useful, the narrowband nature of this approach can: 1) limit the dynamic range of such diagnostics (3), 2) complicate measurements of molecules with broad spectra (e.g., at high pressures), and 3) often prevents multispecies measurements using a single light source. To address these issues, numerous researchers have developed broadband LAS diagnostics, typically with 10s to 1000s of cm$^{-1}$ of spectral bandwidth (4–11).

One common broadband LAS technique employs scanned-wavelength lasers with broad wavelength-tuning capabilities. For example, Sanders et al. (4) used a vertical-cavity surface-emitting laser (VCSEL) to scan $\approx 30$ cm$^{-1}$ near 760 nm in order to acquire measurements of temperature and O$_2$ at 500 Hz in high-pressure gases. More recently, a MEMS-VCSEL capable of tuning $\approx 170$ cm$^{-1}$ near 1.4 $\mu$m has been used to measure temperature and H$_2$O at 100 kHz in a wide variety of combustion applications (see (5) and references therein). In addition, external-cavity quantum-cascade lasers in the mid- and far-IR with large-amplitude ($\approx 100$ cm$^{-1}$) tuning have emerged, which recently enabled measurements of C$_2$H$_4$ between 8.5 and 11.7 $\mu$m in shock-heated gases with a time resolution of 3 ms (6). Unfortunately, light sources suitable for this approach are limited to only a few wavelength regions and the time-resolution is limited to the reciprocal of the scan frequency (typically on the order of 1 ms to 10 $\mu$s).

Numerous techniques employing ultrafast lasers (i.e., lasers emitting ultrashort, typically < 10 ps, pulses) have also been used for broadband LAS measurements of combustion gases, however they have not been applied in the mid-infrared. For example, Sanders (7) used a femtosecond-fiber-laser-pumped supercontinuum source and a scanning bandpass filter to produce 1000 cm$^{-1}$ of bandwidth near 1450 nm for measurements of temperature and several species (H$_2$O, CO$_2$, C$_2$H$_2$, C$_2$H$_6$O) at 50 kHz. More recently, Blume and Wagner (8) used a commercial supercontinuum light-source with a dispersing fiber to acquire measurements of CH$_4$ and temperature at 200 Hz using 110 cm$^{-1}$ of bandwidth near 1650 nm. One drawback to this approach is the relatively large noise levels inherent to supercontinuum light-sources which has prevented single-shot measurements. Recently, Draper et al. (10) applied a dual-frequency-comb spectrometer to characterize combustion environments. The authors used 160 cm$^{-1}$ of bandwidth near 1655 nm to measure temperature and CH$_4$ concentration in a rapid compression machine. Currently, multi-shot averaging and filtering have extended the repetition rate to $\approx 1.4$ kHz (10). Most recently, time-resolved, optically gated absorption (TOGA) spectroscopy was developed by Stauffer et. al. (11) to provide background-free measurements of absorption spectra. The authors used an amplified Ti:Sapphire laser and two frequency-doubling processes to produce 100-fs pulses centered near 310 nm with over 300 cm$^{-1}$ of bandwidth to acquire spectra of OH.

Here we demonstrate the first, to our knowledge, ultra-
fast, single-shot, mid-infrared LAS diagnostic for temperature and species measurements in combustion gases. In addition to the aforementioned potential advantages of broadband LAS diagnostics (e.g., improved high-pressure capability, high-dynamic range, multi-species measurements), we demonstrate that this diagnostic offers several unique advantages: 1) ultrafast (<1 ps) time resolution, 2) access to strong fundamental absorption bands located throughout the mid-wave infrared (2 to 5.5 µm) using a single light source and camera, and 3) potential for single-shot, spatially resolved (1D) thermometry and species measurements at 5 kHz. This manuscript describes the design and operating principles of this diagnostic technique, in addition to its initial validation and application to characterizing flames. Specifically, single-shot, 5 kHz measurements of temperature and CO were acquired in a laser-ignited HMX flame using wavelengths near 4.9 µm, and measurements of temperature and CH₄ were acquired in a partially premixed CH₄-air Hencken-burner flame using wavelengths near 3.3 µm. The results demonstrate that this diagnostic is capable of providing high-precision measurements of temperature (<1%) and molecular species (<2.5%) in combustion gases with ultrafast (<1 ps) time resolution.

**Experimental Procedure**

The experimental system and data processing procedures are summarized in Fig. 1. Ultrafast laser pulses were generated by a mode-locked Ti:Sapphire laser (Coherent Mantis) at a rate of 80 MHz and a center wavelength near 800 nm. The pulses were tailored by a Femtojock pulse-shaper to prepare them for amplification by a multi-stage regenerative chirped-pulse amplifier (Coherent Legend Elite Duo). The amplifier produced pulses with a pulse energy of 2 mJ and duration of 55 fs at a repetition rate of 5 kHz. Next, the pulses were directed into an optical parametric amplifier (OPA) module (Coherent OPerA Solo) equipped with non-collinear difference-frequency generation (NDFG) crystals to generate ultrashort mid-IR pulses. The mid-IR pulses contain ≈600 cm⁻¹ of useful spectral bandwidth and the center wavelength can be tuned between 2.5 and 18 µm via computer controlled manipulation of the crystals. For the results presented here, the pulse energies were 30 µJ and 4 µJ for wavelengths near 3315 nm and 4858 nm, respectively. A MgF₂ Rochon prism polarizer was used to attenuate the pulse energy to ≈0.75 µJ to prevent camera saturation. Next, the mid-IR pulses were directed through the test gas and then focused onto the slit of an Andor Shamrock 500i imaging spectrometer using a cylindrical lens (ZnSe, 50 mm focal length). A 300 groove/mm diffraction grating was used to spectrally disperse the pulses and a Telops FAST-IR 2k high-speed IR camera was used to image each individual pulse in 2D. This configuration provided a theoretical spectral resolution and bandwidth of 0.21 nm and 38 nm, respectively, and similar metrics were achieved in practice. The IR-camera recorded 52x256 pixels with a 5 µs exposure time at 10k frames-per-second in order to record two images per pulse (one for the pulse, another to image background emission between pulses). The camera was synchronized with the laser

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Fig. 2. Images of and pertinent dimensions for the a) laser-ignited HMX flame and b) partially premixed CH₄-air flame studied here.
CO and CH$_4$ were chosen for the initial application of this diagnostic primarily to demonstrate its ability to measure gas properties via molecules with well isolated lines (CO) or blended spectra (CH$_4$). Measurements were acquired in CO’s P-branch near 2060 cm$^{-1}$ due to favorable absorbance levels, lack of interference from other combustion relevant species (e.g., H$_2$O, CO$_2$), and previous combustion studies demonstrating the utility of this spectral region (12–15). Temperature and CH$_4$ measurements were acquired via CH$_4$’s Q-branch near 3015 cm$^{-1}$ due to its strength, isolation from interfering absorption lines, and the large number of transitions with unique lower-state energy comprising it which enhances temperature sensitivity (1, 3).

The center wavelength of the spectrograph and light source were set to 4858 nm for measurements of temperature and CO concentration. Measurements were acquired in a static-gas cell (16) (9.4 cm path length) filled with a commercially prepared gas mixture (2% CO, 1.8% CO$_2$ and 96.2% N$_2$ by mole) at 1 atm and 296 K to validate the accuracy of the diagnostic and data processing routine. Measurements of temperature and CO column density ($\chi_{CO} L$) were also acquired in a laser-ignited HMX flame (see Figure 2a). The HMX was pressed into a 6 mm diameter, 3 mm tall cylindrical pellet and ignited with a CO$_2$ laser emitting 78 W/cm$^2$ at a wavelength of 10.6 µm for the entire test duration. For this test, the $1/e^2$ diameter of the ultrafast beam was reduced from 7.9 mm to 1.4 mm via a lens telescope consisting of a CaF$_2$ plano-convex lens ($f=150$ mm) and an AR-coated Si plano-convex lens ($f=25.4$ mm). The measurement was acquired 7.5 mm above the initial surface location of the pellet.

The accuracy of the temperature and CH$_4$ diagnostic was also validated via measurements in a static-gas cell (0.7 cm path length) and Figure 1 illustrates an example single-shot measurement of CH$_4$’s Q-branch at 296 K and 1 atm. The cell was filled with a commercially prepared mixture of 7% CH$_4$, 15% C$_2$H$_2$ and 78% N$_2$ by mole at 1 atm and 296 K. Measurements were also acquired in a laminar, partially-premixed CH$_4$-air flame (see Figure 2b). The flame was produced by a Hencken burner with a 38.1 mm square core consisting of a honeycomb of alternating jets of CH$_4$ and air surrounded by a 6.4 mm thick co-flow of air. The core-flow equivalence ratio was 6.4 with an exit plane velocity of $\approx$0.9 cm/s.

For each experiment, the measured spectral absorbance ($\alpha$) was calculated at each frequency ($\nu$) using the measured incident ($I_o$) and transmitted ($I_t$) laser intensity and Beer’s Law: $\alpha(\nu) = -\ln[I_o(\nu)/I_t(\nu)]$. $I_o$ was obtained empirically by recording and averaging (to reduce noise) 200 images of ultrashort mid-IR pulses in the absence of the test gas. The signal-to-noise ratio (SNR) of $I_o$ was then further increased by averaging 8 to 18 (depending on test) spectra of $I_o$ (acquired by adjacent rows of pixels within a single image) together. For the results reported here, this corresponds to spatial averaging across less than 1 mm (vertically) at the measurement location in the flame gas.

The gas temperature and absorbing-species concentration were determined by least-squares fitting a simulated absorbance spectra to the measured absorbance spectra. The fitting routine employs the following free parameters: temperature, absorbing species concentration, a frequency shift, and a scaling factor for $I_o$ to account for shot-to-shot fluctuations in pulse energy. The frequency axis of the data was determined by matching 3 to 4 prominent absorption features to their linecenter frequencies (provided by a spectroscopic database) and fitting a linear frequency axis to those points. Absorbance spectra were simulated in the fitting routine using the following procedure: 1) A high-resolution ($\approx 0.0005$ cm$^{-1}$) absorbance spectrum was simulated using $\alpha_{HR}(\nu) = \sum_j S_j(T)\phi_j(\nu)P(\nu)\chi_{L}L$ and a spectroscopic database where $S_j$ and $\phi_j$ are the linestrength and lineshape of transition $j$, respectively, $T$ is the gas temperature, $P$ is the gas pressure, $\chi$ is the absorbing species mole fraction and $L$ is the path length through the absorbing gas. Transition lineshapes were modeled as a Voigt profile. 2) The resolution of the empirical baseline was increased to match that of $\alpha_{HR}$ via linear interpolation, thereby yielding $I_o_{HR}$. 3) Next, Eq. 1 was used to produce a high-resolution, semi-empirical transmission spectrum ($I_o_{HR,cons}$), which has been convolved with
the IRF of the spectrograph-camera setup. 4) \( I_{o, HR} \) was then convolved with the IRF to yield \( I_{o, HR, conv} \). 5) A simulated absorbance spectrum with the IRF accounted for was then calculated from \( I_{o, HR, conv} \) and \( I_{t, HR, conv} \) using Beer’s Law and then downsampled to the same frequency axis as the measured absorbance spectrum to enable direct comparison and the sum-of-squared error (the optimization parameter) to be computed by the fitting routine.

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I_{t, HR, conv}(\lambda) = \int_{-\infty}^{\infty} IRF(\lambda - \tau) \times e^{-\alpha_{HR}(T, P, \chi, L)} d\tau \quad (1)
\]

Here, \( \lambda \) is the wavelength and \( \tau \) is the convolution shift variable. The IRF was modeled as a Lorentzian lineshape.

It is important to note that the IRF is not directly convolved with the simulated absorbance spectrum because the spectrograph-camera setup “sees” a transmission spectrum, not an absorbance spectrum. The convolution with the IRF was executed in wavelength-space where the full-width at half maximum (FWHM) of the IRF is constant. The spectroscopic model for CO employed the HITEMP 2019 database (17) and the spectroscopic model for \( \text{CH}_4 \) utilized a preliminary version (yet to be openly released) of the HITEMP 2019 database for methane (17) which is based on work by Rey et. al. (18).

Results and Discussion

Measurements of temperature and CO concentration in static-gas cell experiments were accurate within 1.5% and 1.8% of known values, respectively, with a 1-\( \sigma \) precision of 0.7% and 1.2%, respectively. Figure 3a displays a representative measured and best-fit absorbance spectra acquired in the HMX flame during quasi-steady-state. The 1-\( \sigma \) noise level in the measured absorbance was 0.25%. Time histories of temperature and \( \chi_{CO}L \) are shown in Figure 3b. The diagnostic resolved pre-ignition decomposition of HMX through quasi-steady burning. At quasi-steady-state, the measured time-averaged temperature and CO column density was 2620 K and 0.32 cm (i.e., 21.3% by mole for a 1.5 cm thick flame) respectively, which agree well with measurements acquired in our lab using quantum-cascade lasers similar to as reported in (14). The 1-\( \sigma \) precisions are 10 K (0.4%) and 0.007 cm (2.3%). Throughout the burn, the temperature decreased by \( \approx 100 \) K due to the surface of HMX regressing away from the measurement line-of-sight. Large amplitude oscillations in \( \chi_{CO}L \) are observed at 12.8 Hz as a result of a natural flame instability (19). Temperature measurements acquired prior to ignition were enabled by the broad spectral bandwidth of the measurement. Measurements with an absorbance SNR as low as 20 were made, which occurred at a CO column density of 0.003 cm and temperature of 500 K.

The temperature and \( \text{CH}_4 \) concentration measured in static-gas cell experiments were accurate within 1.2% and 0.8% of known values, respectively, with a 1-\( \sigma \) precision of 0.2% and 0.7%, respectively. Figure 4a shows a typical single-shot absorbance spectra of \( \text{CH}_4 \)’s Q-branch and Figure 4b shows measured time histories of temperature and \( \text{CH}_4 \) column density acquired in a partially-premixed \( \text{CH}_4 \)-air Hencken-burner flame. The time-averaged values of temperature and column density are 1023 K and 0.283 cm, both of which exhibit a 95 Hz oscillation (due to a combustion instability) with a peak-to-peak amplitude of 28 K and 0.01 cm, respectively. After accounting for this oscillation, the 1-\( \sigma \) precision of the measured temperature and column density are 3 K (0.3%) and 0.003 cm (1%), respectively. The results shown were acquired with an absorbance-noise level of \( \approx 0.5 \)%

The results presented in this manuscript illustrate that ultrafast-laser-absorption spectroscopy in the mid-infrared is capable of high-fidelity characterization of combustion gases with ultrafast time resolution.

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