Time-Dependent Density Functional Theory Investigation on the Electronic and Optical Properties of Poly-C,Si,Ge-acenes

Paola Mocci, Giuliano Mallocci,* Andrea Bosin, and Giancarlo Cappellini*

ABSTRACT: We report a comparative computational investigation on the first six members of linear poly-C,Si,Ge-acenes \(X_{4n+2}H_{4n} (X = C,Si,Ge; n = 1, 2, 3, 4, 5, 6)\). We performed density functional theory (DFT) and time-dependent DFT calculations to compare morphological, electronic, and optical properties. While C-acenes are planar, Si- and Ge-acenes assume a buckled configuration. Electronic properties show similar trends as a function of size for all families. In particular, differently from C-based compounds, in the case of both Si- and Ge-acenes, the excitation energies of the strongest low-lying electronic transition (\(\beta\) peaks) span the visible region of the spectrum, demonstrating their size tunability. For all families, we assessed the plasmonic character of this transition and found a linear relationship for the wavelength-dependence of the \(\beta\) peaks as a function of the number of rings. A similar slope of about 56 nm is observed for Si- and Ge-acenes, although the peak positions of the former are located at lower wavelengths. Outcomes of this study are compared with existing theoretical results for 2D lattices and nanoribbons, and experiments where available.

INTRODUCTION

The discovery of graphene in 2004\(^1\) has opened the way to the synthesis of new 2D-materials. The exotic properties of graphene led shortly after to the further exploration of its silicon and germanium counterparts, respectively known as silicene and germanene.\(^2\)\(^3\) In fact, while these IV-group elements are very similar,\(^4\) each one is characterized by significant peculiarities.\(^5\) Due to the presence of buckling motifs deviating from the planar 2D configuration,\(^6\) in their infinite structural appearance, silicene and germanene appear more easily integrable with substrates than graphene.\(^7\) In addition, these materials exhibit favorable mechanical, electronic, and optical properties,\(^8\) making them ideal systems both for fundamental research and for promising nanoelectronic applications.\(^9\)\(^-\)\(^11\)

As to finite-sized compounds, linear poly-C-acenes composed of fused benzene rings\(^12\)\(^-\)\(^15\) are widely used as active elements in many optoelectronic devices, ranging from photovoltaic cells, light-emitting diodes, flexible and transparent displays, liquid crystals, and organic thin-film field-effect transistors.\(^16\)\(^-\)\(^21\) Analogs of these carbon-based compounds have consequently been targeted for decades. In particular, a large number of computational studies have been performed on Si-based aromatic molecules. As an example, the simplest member hexasilabenzene Si\(_6\)H\(_6\) was first predicted to have a planar \(D_{6h}\) benzene-like structure on the basis of semi-empirical calculations,\(^22\) and then a chair-like \(D_{4d}\) conformation\(^23\) according to ab initio calculations. Structural transition from non-planar to planar conformations in the Si\(_{6-n}\)C\(_n\)H\(_6\) \((n = 0\)–\(6\)) series was later investigated using higher-level coupled cluster methods, showing that deviation from planarity in hexasilabenzene is caused by the pseudo-Jahn–Teller effect.\(^24\) Further computational investigations on poly-Si,Ge-acenes\(^25\)\(^-\)\(^27\) and silicene or germanene nanoribbons have been published over the years.\(^28\)\(^-\)\(^34\)

From the synthesis point of view, reactions involving generation of sila-aromatic compounds, namely silabenzene,\(^35\) 1-silanaphthalene,\(^36\) 2-silanaphthalene,\(^37\) and a 9-silanthracene derivative,\(^36\) have been reported. More recently, an X-ray diffraction study complemented by nuclear magnetic resonance and hybrid density functional theory calculations revealed a tricyclic aromatic isomer of hexasilabenzene with a chair-like silicon frame.\(^39\)

Given the broad interest in heavy analogs of C-based compounds, in this work, we consider the Si- and Ge-acenes analogues of the widely investigated C-based linear acenes;\(^12\)\(^-\)\(^15\) in particular, we focus on the first six members \(X_{4n+2}H_{4n+4} (X =\) planar to
C, Si, Ge; n = 1, 2, 3, 4, 5, 6. Morphological, electronic, and optical properties obtained via (time-dependent) density functional theory (DFT) are presented and discussed comparatively. We highlight the similarities and differences between families as well as the characteristic trends within families as a function of molecular size. We additionally compare our findings with previous theoretical results for the infinite 2D lattices and nanoribbons and with the available experimental data. A web-based repository with input and output files of our simulations is freely available at https://www.dsf.unica.it/csige.

## RESULTS AND DISCUSSION

A 2D sketch of the systems under investigation is shown in Figure 1.

### MORPHOLOGICAL PROPERTIES

From a morphological point of view, an inspection of the DFT-optimized geometries reveals that poly-C-acenes, as expected, maintain the planar geometry typical of the family. On the contrary, all of the investigated poly-Si, Ge-acenes display considerable out-of-plane displacements (buckling). The qualitative comparison is shown in Figure 2 for the representative case of the 3-ring systems.

The average displacements with respect to the molecular plane are reported in Table 1 as a function of the number of rings, together with the values calculated for the 2D infinite lattice, and for H-saturated armchair nanoribbons ASiNR- and AGeNR. While the deviations registered for Si-acenes in the range n = 1—6 appear to be constant along the series, for the corresponding Ge counterparts, a slight decrease at increasing molecular size can be observed. On average, poly-Ge-acenes deviate from planarity more than poly-Si-acenes, with average deviations of about 0.307 and 0.197 Å, respectively. The above results can be compared with those obtained for the corresponding 2D infinite systems (silicene and germanene), also shown in Table 1. In particular, we found that the relative deviations with respect to the corresponding 2D lattice are of the same order of magnitude, about ∼13% for both Si and Ge. In addition, the displacement shown by the heavier compounds is very close to the buckling amplitude calculated for H-saturated armchair nanoribbons ASiNR- and AGeNR.

Figure 3 shows the buckling profile for X₄ₓH₂₆ₓ with X = Si, Ge and n = 1, 2, 3, 4, 5, 6 along the long-axis direction, i.e., the absolute value of the out-of-plane displacement of Si and Ge atoms. We report only the independent displacements for each compound, the others being fixed by symmetry. Atoms are labeled from 1 to 7 according to their position, as marked on the molecule top view at the bottom; atom position 1 (leftmost) is always the outermost. Buckling is not constant, with the obvious exception of one-ring molecules, and shows very similar trends for Si and Ge. Within a single molecule, the displacement shows a kind of oscillatory behavior, which “damps” moving from outer to inner rings (for molecules with three to six rings), Si damping being faster than Ge. This is not completely unexpected given that inner rings, at least in one direction, are somehow more constrained with respect to outer ones. Note that for the latter, the profile is a flat line since the absolute out-of-plane displacements are virtually constant.

Table 2 compares our computed C–C, Si–Si, and Ge–Ge bond lengths for the smallest and largest compounds (n = 1 and n = 6) to available data for Si₆H₆, Si₂H₄, and 3D lattices, ASiNR, ASiNR-9, and AGeNR-9 nanoribbons. Si–Si and Ge–Ge bond length profiles are additionally depicted in Figure 4 for the heaviest systems X₄ₓH₂₆ₓ with X = C, Si, Ge. Bonds are labeled from A to J according to their position, as marked on the molecule top view at the bottom; bonds A and G (leftmost) are always the outermost. Excluding the absolute values, the
behavior is very similar for C, Si, and Ge, and for bonds A–F shows a damped oscillation somehow similar to buckling amplitudes in Figure 3. On the contrary, bonds G to J exhibit a saturating behavior when going from outer to inner rings.

In summary, both buckling and bond profiles indicate that inner rings are more “regular” than the outer ones. Compared with the 2D lattice,

| n     | C    | Si    | Ge    |
|-------|------|-------|-------|
| 6 (outer ring) | 1.36–1.45 | 2.21–2.27 | 2.33–2.40 |
| 6 (inner ring) | 1.40–1.45 | 2.25–2.30 | 2.38–2.42 |

Silo-benzene

| n     | C    | Si    | Ge    |
|-------|------|-------|-------|
| 15    |      | 2.23  |       |

2D lattice

| n     | C    | Si    | Ge    |
|-------|------|-------|-------|
| 1     | 1.39 | 2.23  | 2.36  |
| 6 (outer ring) | 1.36–1.45 | 2.21–2.27 | 2.33–2.40 |
| 6 (inner ring) | 1.40–1.45 | 2.25–2.30 | 2.38–2.42 |

Silo-benzene

| ![Figure 3. Profile of absolute out-of-plane displacements (buckling) for X₄₋₄H₂₋₄, with X = Si,Ge and n = 1, 2, 3, 4, 5, 6 for the atoms labeled as shown at the bottom.](image)
| ![Table 2. Bond Lengths (Å) for Selected Poly-C,Si,Ge-acenes](image) |

### ELECTRONIC PROPERTIES

The computed vertical electron affinity $E_{A}$, vertical ionization energy $E_{i}$, fundamental gap $E_{gap}$, and HOMO–LUMO gap $E_{HL}$ for the different systems considered are reported in Tables 3–5 and compared with previous calculations and available experimental data. The behavior of these quantities as a function of molecular size is shown in Figure 5. As expected, in all cases,
Table 3. Vertical Electron Affinity (E_{A_v}), Vertical Ionization Energy (E_{I_v}), Fundamental Gap (E_{gap} = E_{I_v} - E_{A_v}), and HOMO–LUMO Gap (E_{HL}) for the Poly-C-acenes C_{n+2}H_{2n+4}, n = 1, 2, 3, 4, 5, 6

| n   | E_{A_v} | E_{I_v} | E_{gap} | E_{HL} |
|-----|---------|---------|---------|--------|
| This Work |        |         |         |        |
| 1    | −1.64 (−1.39) | 9.32 (9.20) | 10.96 (10.59) | 6.74 (6.60) |
| 1 (exp) | −1.12 ± 0.03 | 9.2438 ± 0.00006 | 10.36 | 6.90 |
| 2    | −0.39 (−0.38) | 8.01 (7.89) | 8.40 (8.27) | 4.82 (4.74) |
| 2 (exp) | −0.20 ± 0.05 | 8.144 ± 0.001 | 8.34 | 4.45 |
| 3    | 0.46 (0.43) | 7.20 (7.09) | 6.74 (6.66) | 3.60 (3.54) |
| 3 (exp) | 0.530 ± 0.005 | 7.439 ± 0.006 | 6.91 | 3.45 |
| 4    | 1.04 (1.00) | 6.65 (6.55) | 5.61 (5.55) | 2.78 (2.74) |
| 4 (exp) | 1.067 ± 0.043 | 6.97 ± 0.05 | 5.90 | 2.72 |
| 5    | 1.47 (1.41) | 6.26 (6.16) | 4.80 (4.75) | 2.21 (2.19) |
| 5 (exp) | 1.392 ± 0.043 | 6.589 ± 0.001 | 5.20 | 2.31 |
| 6    | 1.79 (1.72) | 5.97 (5.87) | 4.18 (4.15) | 1.80 (1.78) |
| 6 (exp) | 6.36 ± 0.02 | 5 | 1.90 | |

H-Saturated Nanoribbons
−ZGNR^{42}
−ZGNR^{28}
2D and 3D Lattices
2D \[ \text{(exp)} \] \[ \text{(exp)} \] 4.61 4.61 0 5.4

*Results from previous B3LYP/6-31 + G* calculations (between parentheses) and available experimental data as compiled in ref 12 are reported. All energies are expressed in eV.

Table 4. Vertical Electron Affinity (E_{A_v}), Vertical Ionization Energy (E_{I_v}), Fundamental Gap (E_{gap}), and HOMO–LUMO Gap (E_{HL}) for the Poly-Si-acenes Si_{n+2}H_{2n+4}, n = 1, 2, 3, 4, 5, 6

| n   | E_{A_v} | E_{I_v} | E_{gap} | E_{HL} |
|-----|---------|---------|---------|--------|
| This Work |        |         |         |        |
| 1    | 1.22 | 7.42 | 6.20 | 3.22 |
| 2    | 2.00 | 6.73 | 4.74 | 2.26 |
| 3    | 2.50 | 6.32 | 3.81 | 1.68 |
| 4    | 2.84 | 6.04 | 3.20 | 1.31 |
| 5    | 3.08 | 5.85 | 2.76 | 1.06 |
| 6    | 3.26 | 5.70 | 2.44 | 0.88 |

H-Saturated Nanoribbons
2-ZSiNR^{29} 0.25
2D and 3D Lattices
2D \[ \text{lattice} \] \[ \text{(exp)} \] \[ \text{(exp)} \] 4.76 4.76 0 0.03 1.17
2D lattice + spin–orbit \[ \text{(exp)} \] \[ \text{(exp)} \] 4.74 4.77 0 0.04 1.17

*All energies are expressed in eV

Table 5. Same as Table 4 for Poly-Ge-acenes Ge_{n+2}H_{2n+4}, n = 1, 2, 3, 4, 5, 6

| n   | E_{A_v} | E_{I_v} | E_{gap} | E_{HL} |
|-----|---------|---------|---------|--------|
| This Work |        |         |         |        |
| 1    | 1.50 | 7.51 | 6.00 | 3.04 |
| 2    | 2.24 | 6.82 | 4.58 | 2.14 |
| 3    | 2.72 | 6.43 | 3.71 | 1.62 |
| 4    | 3.04 | 6.18 | 3.14 | 1.28 |
| 5    | 3.26 | 6.00 | 2.74 | 1.06 |
| 6    | 3.42 | 5.86 | 2.44 | 0.91 |

2D and 3D Lattices
2D \[ \text{lattice} \] \[ \text{(exp)} \] \[ \text{(exp)} \] 4.46 4.46 0 0.04 0.744

As shown in Table 3, the present results for poly-C-acenes are consistent with previously reported data, 12,15,63 the small differences (at most 2%) being due to the different combinations exchange-correlation functional/basis sets adopted; more importantly, the obtained results are in fair agreement with the experimental data available (compiled in refs 12,15 and reported in Table 3). Note that, in particular, while for poly-C-acenes we find negative values for the EA, of the first two members benzene and naphthalene, in the case of poly-Si,Ge-acenes, the electron affinities are always positive.

As a consequence of the above trends, the fundamental gap \( E_{gap} \) decreases as a function of size. More specifically, the relative deviations calculated with respect to the first member of each family reveal a reduction of \( E_{gap} \) of the same order of magnitude in all cases (from −62 to −23, −61 to −23, and −59 to −24% for poly-C,Si,Ge-acenes, respectively). Note that the HOMO–LUMO gaps calculated for poly-Si-acenes \( Si_{n+2}H_{2n+4} \) are in perfect agreement with the results of ref 8 obtained at the same level of theory.

As shown in Tables 3–5, EA and IE have been calculated for graphene, silicene, and germanene 2D lattices, 40 which are zero gap materials, so EA and IE are the same, and lie approximately midway between our EA/IE values. One could be tempted to argue that \( E_{gap} \) and \( E_{HL} \) for large values of \( n \) tend to the values calculated for 2D lattices, 40 which show zero gap or, for Si and Ge, very small gaps if spin–orbit coupling is taken into account (see Tables 4 and 5). Unfortunately such a conclusion is not justified, due to finite size effects in the short direction of the molecules, as witnessed by the results obtained for hydrogen-saturated nanoribbons, which may show a zero or non-zero band gap depending on the ribbon width or edge shape. Indeed, for large values of \( n \), \( X_{n+2}H_{2n+4} \) closely resembles 2-ZXR nanoribbon structures. 28 First-principles calculations on the latter give a direct gap 0.25 eV wide for \( X = Si^{29} \) and −0.2 eV wide for \( X = C \) (graphene). 42 The above absolute values should be
taken only as estimates due to the well-known gap underestimation problem. Interestingly, other works on 2-ZGNR predict a zero gap.

**OPTICAL PROPERTIES**

Following the notation adopted for poly-C-acenes, in Table 6, we report the main peak energy and oscillator strength of the so-called $\beta$ and $p$ bands. The $\beta$ and $p$ bands correspond to the main peak and the optical onset of the absorption spectrum, respectively. The $\alpha$ band, on the contrary, is characterized by a negligible oscillator strength, which makes this transition usually non-detectable in the absorption spectrum.

The last column of Table 6 reports the exciton binding energy $E_{\text{bind}}$ estimated as the difference between the fundamental gap $E_{\text{gap}}$ and the optical gap $E_{\text{opt}}$, which corresponds to the $p$ band energy. As expected, a general reduction of $E_{\text{bind}}$ is observed in all cases as a consequence of a general decrease of confinement effects and reduction of screening as the molecular size increases. Interestingly, while the relative reduction is roughly preserved along the three families (in the range from $-20$ to $-50\%$), the values for poly-Si,Ge-acenes are almost coincident and on average smaller by about $30\%$ with respect to the corresponding value for poly-C-acenes. The above results show that, at a fixed molecular size, poly-Si,Ge-acenes support less bounded excitons with respect to poly-C-acenes. This can be ascribed to the different interplay between the two ingredients entering $E_{\text{bind}}$, i.e., $E_{\text{gap}}$ (which is larger for poly-C-acenes) and the optical onset (the energy of the $p$ band) for C-acenes on one side and poly-Si,Ge-acenes on the other.

Figure 5. Computed electronic properties as a function of size. Vertical electron affinity (EA, ) and vertical ionization energy (IE, ) are reported in the left panel, while the fundamental gap $E_{\text{gap}}$ is shown in the right panel. Adopted color codes are red, blue, and orange for poly-C,Si,Ge-acenes, respectively.

Table 6. Energies (eV) of the $p$, $\alpha$, and $\beta$ Peaks as a Function of Molecular Size as Obtained Via TD-DFT Calculations for the Poly-C,Si,Ge-acenes Considered $X_{4n+2}H_{2n+4}$, with $n = 1$, 2, 3, 4, 5, 6

| $X_{4n+2}H_{2n+4}$ | $p$ | $\alpha$ | $\beta$ | $E_{\text{bind}}$ |
|------------------|-----|---------|-------|--------------|
| C$_{4n+2}H_{2n+4}$ | 5.50/4.73 ($<0.01$) | 6.22/5.96 ($<0.001$) | 7.19/6.64 ($1.20$) | 4.75 |
| Si$_{4n+2}H_{2n+4}$ | 2.84 (0.02) | 2.46 ($<0.001$) | 3.39 (0.69) | 3.36 |
| Ge$_{4n+2}H_{2n+4}$ | 2.66 (0.03) | 2.28 ($<0.001$) | 3.17 (0.55) | 3.34 |

The corresponding oscillator strengths are reported within parentheses. The last column reports the exciton binding energies $E_{\text{bind}}$ with percentage deviation with respect to corresponding value of the smallest member in each class. All results have been obtained using B3PW91/TZVP, except for those marked with * achieved with BP86/TZVP and with † which are experimental values.

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In previous works on polyacenes\textsuperscript{12,15,45} it has been found that both $\beta$ and $\alpha$ peaks correspond to transitions polarized along the main molecular axis, while the $p$ band is polarized along the perpendicular direction. Such a behavior for $p$, $\alpha$, and $\beta$ is confirmed here, not only for C but also for Si and Ge (transition dipole moment data are not shown, but are available in the

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**Figure 6.** Comparison between the computed absorption cross section (Mb) and the previously published theoretical (ref 12) and experimental data (compiled in ref 14) for poly-C-acenes C, $n = 1, 2, 3$, from top to bottom, respectively.

**Figure 7.** Absorption cross section (a.u.) for poly-C-acenes C$_{4n+2}$H$_{2n+4}$, $n = 1, 2, 3, 4, 5, 6$, from top to bottom, respectively.
Supporting Information of ref 46). The data reported for \( p \), \( \alpha \), and \( \beta \) bands of poly-C-acenes agree with those previously obtained at a different level of theory (B3LYP/6-31 + G\(^*\))\(^\text{12,14,15} \) and are in fairly good agreement with the available experimental data\(^\text{18} \) (marked with b in Table 6). As an example, Figure 6 compares the absorption spectra for the first three members of the poly-C-acenes class.

Figure 8. Absorption cross section (a.u.) for poly-Si-acenes \( \text{Si}_{4n+2}\text{H}_{2n+4} \), \( n = 1, 2, 3, 4, 5, 6 \). The visible range is highlighted.

Figure 9. Absorption cross section (a.u.) for poly-Ge-acenes \( \text{Ge}_{4n+2}\text{H}_{2n+4} \), \( n = 1, 2, 3, 4, 5, 6 \). The visible range is highlighted.
Comparison of the results for poly-Si-acenes with ref 48 reveals that our α and β peaks are located at energies ∼0.25 eV higher, as expected due to the different exchange-correlation functional adopted (BP86 in ref 48, B3PW91 in the present work). We indeed verified for Si_{10}H_{16} and Si_{26}H_{16} that TD-DFT calculations at the BP86/TZVP level of theory (marked with a in Table 6) make our data virtually coincident, within numerical errors, with those of ref 48.

As expected, and consistently with previous findings, we found in all cases that the energy of the main transitions decreases as a function of molecular size, while the corresponding oscillator strength increases. This is clearly seen in Figures 7–9, displaying the absorption spectra up to the near-UV of all the species considered. Inspection of the above figures confirms visually the main trend previously observed for all families: a general red shift of the optical onsets and the dominant peaks as a function of the molecular dimension. In addition, for C-acenes, the strongest β transition always has B_{2u} symmetry, while the symmetry of the most important higher energy peaks (oscillator strength greater than 0.1) changes from B_{1u} (polarization perpendicular to the long axis) to B_{2u} (polarization aligned with long axis) when n increases from 2 to 6. Similarly, Si- and Ge-acenes show A_{g} symmetry for the strongest β peaks, and we observe a shift from B_{u} (polarization perpendicular to the long axis) to A_{g} (polarization aligned with long axis) for the higher energy transitions when the size of the molecule increases. The complete sets of 50 electronic transitions, computed at the TD-DFT level, for all poly-C,Si,Ge-acenes with n = 2, 3, 4, 5, 6, are available in the Supporting Information of ref 46.

In particular, it is instructive to compare the positions of the strongest features in the absorption spectra for the three families considered. Figure 10 displays, as a function of molecular size,

![Figure 10](image)

The main absorption peaks for C-acenes fall in the UV part of the spectrum, while for poly-Si,Ge-acenes, this is true only for the smallest cluster. As observed elsewhere for both poly-Si,Ge-acenes, the excitation energies of the β peaks span the visible region of the spectrum, and this demonstrates the tunability of these systems as a function of size. In addition, as already shown for polyacenes and poly-Si-acenes,8,49 we find in all cases that the same transitions contribute to α and β peaks (e.g., HOMO → LUMO+1 and HOMO-1 → LUMO for X_{10}H_{16} and X_{26}H_{16}, X = C,Si,Ge). While in the former case, the addition of transition dipole moments is destructive (similar amplitudes but with opposite signs); in the latter case it is constructive, and this results in low and high oscillator strengths, respectively. This is recognized as the signature of the plasmonic origin of the β peaks. It is interesting to notice that destructive interaction for α peaks decreases (i.e., strength increases) with size.

### CONCLUSIONS

We presented a systematic (TD)-DFT study of the morphological, electronic, and optical properties of poly-C,Si,Ge-acenes (X_{4n+2}H_{4n+4}, X = C,Si,Ge, n = 1, 2, 3, 4, 5, 6). We compared our results with existing theoretical data for 2D lattices and nanoribbons and available experiments. Analysis of the morphological properties confirms previous results; according to which, while C-based acenes are planar, both Si- and Ge-based counterparts assume a buckled configuration. Concerning electronic properties, we found for each family a general increase (decrease) of the vertical electron affinities (ionization energies) as a function of size. This gives rise to an overall closure of the fundamental electronic gap, as expected from quantum confinement effects. Independently of the nature of the atomic constituents, this property is reflected in a general red shift of both the optical onset and the position of the dominant UV-visible absorption peaks, as a function of size. In particular, we found a linear relationship describing the wavelength-dependence of the β peaks with the number of rings and a similar slope of about 56 nm is observed for Si- and Ge-acenes. The present investigation contributes to the search of new, complementary materials for opto-electronic applications and devices.

### COMPUTATIONAL METHODS

Ground-state electronic properties were computed in the framework of the density functional theory.51 Following previous studies on poly-Si-acenes,59,60,62 geometry optimizations were performed using the B3PW91 hybrid exchange-correlation functional,53,54 combined with the TZVP basis-set, a triple-ζ valence basis set with one set of polarization d-functions on heavy atoms and one set of p-functions on hydrogen atoms.55 We computed vertical electron affinities (E_{A}) and ionization energies (E_{I}) via total energy differences by considering the ±1 charged species at the neutral optimized geometry. According to the ΔSCF method,56 the fundamental gap is given by

\[ E_{\text{gap}} = E_{I_e} - E_{A_e} = (E_{N_e} - E_N) - (E_N - E_{N+1}) \]  

\[ E_{\text{IP}} (M = N - 1, N, N + 1) \]  

being the total energy of the M-electron system. To obtain the electronic absorption spectra, we performed time-dependent DFT (TD-DFT)63 calculations at the same level of theory B3PW91/TZVP employed for ground-state calculations. We used the frequency space implementation in which the poles of the linear response function correspond to vertical excitation energies and pole strengths represent oscillator strengths.59 TD-DFT is an efficient and powerful...
scheme for the calculation of the absorption spectra of finite systems, typically yielding results in very good agreement with available experimental data.\textsuperscript{5,60,61} The many-body perturbation theory can be used to compute optical absorption spectra of molecules and clusters.\textsuperscript{62,63} However, while this technique has proven to provide results in very good agreement with high-level quantum chemistry techniques,\textsuperscript{64} it is computationally intensive and not suited for a systematic comparative investigation like the one presented here. We estimate exciton-binding energies $E_{\text{bind}}$ by subtracting the energy of the first optically active transition ($E_{\text{opt}}$) from that of the fundamental gap ($E_{\text{gap}}$): $E_{\text{bind}} = E_{\text{opt}} - E_{\text{gap}}$.\textsuperscript{57,83,65} $E_{\text{bind}}$ is one of the key parameters regulating the optical absorption of materials.\textsuperscript{44} All calculations were performed using the Gaussian-09 software package,\textsuperscript{66} and images were rendered with the VMD software.\textsuperscript{67} Input and output Gaussian files, as well as the list of 50 computed electronic transitions for each molecule are freely available at https://www.dsf.unica.it/csige.

**AUTHOR INFORMATION**

**Corresponding Authors**

Giuliano Malloci — Department of Physics, University of Cagliari, I-09042 Monserrato, CA, Italy; orcid.org/0000-0002-5985-257X; Email: giuliano.malloci@dsf.unica.it

Giancarlo Cappellini — Department of Physics, University of Cagliari, I-09042 Monserrato, CA, Italy; orcid.org/0000-0001-6300-5712

**Authors**

Paola Mocci — Department of Physics, University of Cagliari, I-09042 Monserrato, CA, Italy

Andrea Bosin — Department of Physics, University of Cagliari, I-09042 Monserrato, CA, Italy; orcid.org/0000-0001-9746-302S; Email: andrea.bosin@dsf.unica.it

Complete contact information is available at: https://pubs.acs.org/10.1021/acsomega.0c01516

**Notes**

The authors declare no competing financial interest.

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