In-plane spin excitation anisotropy in the paramagnetic state of NaFeAs

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We use unpolarized and polarized inelastic neutron scattering to study low-energy spin excitations in NaFeAs, which exhibits a tetragonal-to-orthorhombic lattice distortion at \(T_s \approx 58\) K followed by a collinear antiferromagnetic (AF) order below \(T_N \approx 45\) K. In the AF ordered state \((T < T_N)\), spin waves are entirely \(c\)-axis polarized below \(\sim 10\) meV, exhibiting a gap of \(\sim 4\) meV at the AF zone center and disperse to \(\sim 7\) meV near the \(c\)-axis AF zone boundary. On warming to the paramagnetic state with orthorhombic lattice distortion \((T_N < T < T_s)\), spin excitations become anisotropic within the FeAs plane. Upon further warming to the paramagnetic tetragonal state \((T > T_s)\), spin excitations become more isotropic. Since similar magnetic anisotropy is also observed in the paramagnetic tetragonal phase of superconducting BaFe\(_{1.94}\)Ni\(_{0.06}\)As\(_2\), our results suggest that the spin excitation anisotropy in superconducting iron pnictides originates from similar anisotropy already present in their parent compounds.

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I. INTRODUCTION

The parent compounds of iron pnictide superconductors are semi-metallic antiferromagnets exhibiting a tetragonal-to-orthorhombic lattice distortion at temperature \(T_s\) followed by a paramagnetic to antiferromagnetic (AF) phase transition at \(T_N\). The magnetic structure is collinear with the ordered moment aligned antiferromagnetically along the \(a\)-axis of the orthorhombic lattice [Fig. 1(a)]. From transport, resonant ultrasound, angle-resolved photoemission spectroscopy (ARPES), inelastic neutron scattering, magnetic torque, and scanning tunneling microscopy (STM) measurements, it is clear that iron pnictides have electronic anisotropy above \(T_N\) implying an underlying electronic nematic phase. However, the microscopic origin of the observed electronic anisotropy is still an issue of debate. In both the strong and weak coupling limits, the electronic anisotropy could be caused by a spin nematic phase (spin anisotropy) in the paramagnetic orthorhombic phase above \(T_N\) but below \(T_s\). Alternatively, orbital ordering in the paramagnetic orthorhombic state may also induce the observed electronic anisotropy. Although transport and X-ray diffraction experiments in magnetic fields on electron-doped BaFe\(_{2-x}\)Co\(_x\)As\(_2\) reveal clear evidence for anisotropic in-plane static spin susceptibility \((\chi_a \neq \chi_b)\) in the paramagnetic orthorhombic state \((T \leq T \leq T_s)\), it is still unclear if such in-plane susceptibility anisotropy is field-induced or intrinsic to these materials at zero field. Furthermore, recent STM and transport measurements suggest that the resistivity anisotropy in Co-doped BaFe\(_2\)As\(_2\) arises from Co-impurity scatter-
FIG. 1: (Color online) (a) The orthorhombic chemical unit cell of NaFeAs (enclosed by grey lines, two orthorhombic chemical unit cells are stacked along the c-axis), the black arrows indicate directions of the ordered moments and orange spheres represent Fe atoms, Na and As atoms are not shown. (b) Points in reciprocal space probed in this work. The points represent magnetic zone centers (L = 0.5, 1.5) while the crosses represent magnetic zone boundaries (L = 0, 1) along the (1,0,L) direction. The dashed green lines enclose the magnetic Brillouin zone. The relationship between the neutron polarization directions (x, y, z) and the scattering plane are shown in (c) for Q = (1,0,0.5) and in (e) for (1,0,1.5). The angle between x-direction and the H-axis is denoted as θ₁ for (1,0,0.5) and θ₂ for (1,0,1.5). The magnetic components measured in each channel and their relationships to the magnetic components projected onto the crystal axes are shown in (d) for Q = (1,0,0.5) and in (f) for (1,0,1.5). Only SF channels are measured in this work. σ² of contains both Mₐ and Mₜ magnetic components, whereas only Mₐ and Mₜ contribute to σ² and σ², respectively. The relationships between the magnetic components along the neutron polarization directions (Mₐ, Mₜ and Mₕ) and crystal axes (Mₐ, Mₕ, and Mₜ) are shown in the boxes in (d) and (f) for L = 0.5 and L = 1.5 respectively.

\[ \chi''(Q, E)/[1 - \exp(-E/kBT)] \] at the AF wave vector \( E = 6 \text{ meV} \) has in-plane anisotropy with \( Mₐ \geq Mₕ \) in the paramagnetic orthorhombic state (\( T_N \leq T \leq T_s \)) of NaFeAs. Such anisotropy becomes much weaker above \( T_s \) and spin excitations become nearly isotropic. Since the in-plane anisotropic paramagnetic spin excitations in NaFeAs are similar to those observed in the tetragonal phase of superconducting BaFe₁₋₀.₉₆Ni₀₋₀.₉₆As, the spin excitation anisotropy in superconducting iron pnictides originates from similar anisotropy already present in the parent compound. While these results suggest the presence of a spin nematic state in the paramagnetic orthorhombic phase of NaFeAs, they may also be consistent with anisotropic critical fluctuations due to a single-ion anisotropy in the orthorhombic phase.

### II. EXPERIMENTAL RESULTS

Figure 1(a) shows the collinear AF structure of NaFeAs with orthorhombic lattice parameters \( a = 5.589 \), \( b = 5.569 \) and \( c = 6.991 \). We define momentum transfer \( \mathbf{Q} \) in three-dimensional reciprocal space in \( \text{Å}^{-1} \) as \( \mathbf{Q} = H\mathbf{a}^* + K\mathbf{b}^* + L\mathbf{c}^* \), where \( H, K, \) and \( L \) are Miller indices and \( \mathbf{a}^* = 2\pi/a, \mathbf{b}^* = 2\pi/b, \mathbf{c}^* = 2\pi/c \). About 5 grams of single crystals of NaFeAs were coaligned in the \( [H,0,L] \) scattering plane [Fig. 1(b)]. In this notation, the AF Bragg peaks and zone centers occur at \( [1,0,L] \) with \( L = 0.5, 1.5, \cdots \), while the AF zone boundaries along the \( c \)-axis occur at \( L = 0, 1, 2, \cdots \). Our polarized neutron scattering experiments were carried out using the IN22 thermal triple-axis spectrometer at the Institut Laue-Langevin, Grenoble, France. Consistent with previous notation, we define the neutron polarization directions along \( \mathbf{Q} \) as \( x \), perpendicular to \( \mathbf{Q} \) but in the scattering
plane as $y$, and perpendicular to $Q$ and the scattering plane as $z$, respectively [Figs. 1(c) and 1(e)]. Since neutron scattering is only sensitive to magnetic scattering components perpendicular to the momentum transfer $Q$, one can probe magnetic responses within the $y - z$ plane ($M_y$ and $M_z$) [Fig. 1(c)].

Within the scattering plane, the measured magnetic response at $Q$ give $M_y = \sin^2 \theta M_a + \cos^2 \theta M_c$ and $M_z = M_b$, where the angle between $Q$ and $[H, 0, 0]$ is $\theta$, and $M_a$, $M_b$, and $M_c$ are spin excitation intensities along the orthorhombic $a$-, $b$-, and $c$-axis directions, respectively. This is related to the observed neutron spin-flip (SF) scattering cross sections for different neutrons along the orthorhombic $y$-plane via:

$$\begin{align*}
\sigma_x^\text{SF} &= \frac{R}{R+1}(\sin^2 \theta M_a + \cos^2 \theta M_c) + \frac{R}{R+1} M_b + B, \\
\sigma_y^\text{SF} &= \frac{1}{R+1}(\sin^2 \theta M_a + \cos^2 \theta M_c) + \frac{R}{R+1} M_b + B, \\
\sigma_z^\text{SF} &= \frac{R}{R+1}(\sin^2 \theta M_a + \cos^2 \theta M_c) + \frac{1}{R+1} M_b + B
\end{align*}$$

where $R$ is the flipping ratio for non-spin-flip (NSF) and SF scattering ($R = \sigma^\text{NSF}/\sigma^\text{SF} \approx 15$) and $B$ is the background scattering that may be larger than the magnetic scattering. Therefore, to conclusively determine the magnetic anisotropy along the three crystallographic directions $M_a$, $M_b$, and $M_c$ of the orthorhombic lattice, we need to measure neutron SF scattering at two or more equivalent AF wave vectors with different angle between the wave vector $Q$ and $[H, 0, 0]$. To compare the estimated $M_a$, $M_b$, and $M_c$ at different wave vectors, we need to consider in addition the differences in the magnetic form factor $F(Q)$ and instrumental resolution $\sigma$. For example, at the AF zone center $[1,0,0]$ ($L = 0.5, 1.5, \cdots$) positions, by combining the cross sections measured at $Q = (1, 0, 0.5)$ and $Q = (1, 0, 1.5)$ for a particular energy transfer ($\sigma^{SF}_x, \sigma^{SF}_y$ and $\sigma^{SF}_z$ at both wave vectors), we have five quantities ($M_a$, $M_b$, $M_c$ and $B$ at the two wave vectors) to be determined from up to six cross sections [Figs. 1(c)-1(f)]. We either measured all six cross sections and used the over-determination to improve estimates of $M_a$, $M_b$, and $M_c$ [Fig. 3(a)-3(d)] or measured five cross sections which uniquely determines the magnetic response [Fig. 4(c)-4(d)]. A similar procedure is used to analyze data for the zone boundary along the $c$-axis ($L = 0.1$).

In previous unpolarized neutron scattering measurements of spin waves in Na$_0.9$FeAs, the onset of spin gap at the AF zone center $Q = (1, 0, 0.5)$ is observed at approximately $\sim 9$ meV. Figure 2 summarizes our unpolarized neutron measurements on NaFeAs using HB-3 triple-axis spectrometer at the High-Flux-Isotope Reactor (HFIR), Oak Ridge National Laboratory. The monochromator, analyzer, and filters are all pyrolytic graphite. The collimations are 48'-40'-sample-40'-120' with final neutron energy fixed at $E_f = 14.68$ meV. Our energy scan at the AF zone center wave vectors $Q = (1, 0, 0.5)$ reveals a clear spin gap of $\sim 4$ meV [Fig. 2(a)], much smaller than that of Na$_0.9$FeAs$^{37}$. Upon moving the wave vectors to $Q = (1, 0, 0.3), (1, 0, 0.2), (1, 0, 0)$, the spin gap changes to $\sim 7$ meV at the $c$-axis AF zone boundary position with $L = 0$ [Fig. 2(a)]. To understand these data, we fit the spin wave spectra with a damped harmonic oscillator, $\chi''(Q, E) = AE_0(Q) \Gamma E / [(\Gamma E)^2 + (E_0^2 - E^2)^2]$, convolved with instrumental resolution similar to previous works. The spin wave dispersion is $E(Q) = \Delta(1,0,L)^2 + v_x^2 h^2 + v_y^2 k^2$, where $\Delta(1,0,L)$ is the spin gap value, $v_x$ and $v_y$ are spin wave velocities along the $a$- and $b$-axes, respectively. The solid lines in Fig. 2(a) show the fits using spin wave velocities of NaFeAs obtained from high-energy time-of-flight measurements. Figure 2(b) shows the $c$-axis dispersion of the spin waves. Given the almost identical $T_N$ and $T_s$ between our NaFeAs samples and Na$_0.9$FeAs$^{37}$, it is unclear why their spin gap values are so different.

Figure 3 shows the energy scans at the AF zone center $Q = (1, 0, 0.5), (1, 0, 1.5)$ and zone boundary $Q = (1, 0, 0), (1, 0, 1)$ with different neutron polarizations in the low-temperature AF ordered state. At the AF wave vectors $Q = (1, 0, 0.5)$ [Fig. 3(a)], we find a clear spin gap of $\sim 4$ meV consistent with unpolarized data of Fig. 2. Furthermore, $\sigma^{SF}_x$ are similar to $\sigma^{SF}_y$ for $E \lesssim 11$ meV while $\sigma^{SF}_z > \sigma^{SF}_y > \sigma^{SF}_x$ for $E > 11$ meV. Similar results are obtained at $Q = (1,0,1.5)$ [Fig. 3(c)]. In order to...
obtain $M_a$, $M_b$, and $M_c$, we assume Fe$^{2+}$ magnetic form factor and correct for the instrumental resolution factor $r$ at these two wave vectors. The obtained $M_a$, $M_b$ and $M_c$ are shown in Fig. 3(c). We see that spin waves in NaFeAs are transverse to the ordered moment direction and almost entirely $c$-axis polarized with $M_a \approx M_b \approx 0$ for $E \leq 10$ meV [Fig. 1(e)]. This is similar to the low temperature spin waves in BaFe$_2$As$_2$.[22] For spin wave energies above 10 meV, we see a dramatic reduction in $M_a$ and a corresponding increase in $M_b$. Most surprisingly, there appears to be a small, but nonzero $M_b$ around 12 meV, suggesting the possible presence of longitudinal spin excitations. This is disallowed for spin waves in a classical local moment Heisenberg Hamiltonian, but may be present in NaFeAs due to itinerant electrons.[8] Figures 3(b), 3(d) show similar results at the AF zone boundary $Q = (1, 0, 0)$ and $(1, 0, 1)$. The energy dependence of $M_a$, $M_b$, and $M_c$ are shown in Fig. 3(f). Again, spin waves are entirely polarized along the $c$-axis for energies below 10 meV and have no longitudinal component for the probed energy range. We note that recent polarized neutron scattering experiments on BaFe$_2$As$_2$ have conclusively established the presence of longitudinal spin-wave excitations in the AF ordered phase.[22]

FIG. 4: (Color online) Constant-$Q$ scans at $T = 60$ K for $(1,0,0.5)$ and $(1,0,1.5)$ are shown in (a) and (b), respectively. Temperature dependence of the three spin-flip cross sections for the AF zone centers $(1,0,0.5)$ and $(1,0,1.5)$ are shown in (c) and (d). (e) The difference of the magnetic components $M_b$ and $M_c$ for $L = 0.5$ determined from $\sigma_{x}^{SF}$ and $\sigma_{y}^{SF}$ in (c). The temperature dependence of $M_a$, $M_b$, and $M_c$ at the magnetic zone center are determined and plotted in (f). In cases where only cross sections for $L = 0.5$ are measured, only $M_b$ can be determined, when $\sigma_{x}^{SF}$ and $\sigma_{y}^{SF}$ for $L = 1.5$ are in addition measured, all three components along crystal axes can be determined, when all three channels are measured for both $L = 0.5$ and $L = 1.5$, the over-determination is used to improve estimates of $M_a$, $M_b$, and $M_c$. The point at $T \approx 60$ K is obtained by combining raw data from temperatures in the range indicated by horizontal bars and the constant-$Q$ scans in (a) and (b) from $E = 4-8$ meV, the combined $\sigma_{x}^{SF}$, $\sigma_{y}^{SF}$ and $\sigma_{z}^{SF}$ for $L = 0.5$ and $L = 1.5$ are shown in the inset. The solid vertical grey line through (c), (d), (e) and (f) marks the magnetic transition temperature $T_N$ whereas the dashed grey line marks the structural transition temperature $T_s$. The solid lines in (e) and (f) are guides to the eye.

To probe the evolution of spin excitations in the paramagnetic orthorhombic ($T_N \leq T \leq T_s$) and tetragonal ($T > T_s$) phases, we study the temperature dependence of spin excitations at $E = 6$ meV from 2 K to 80 K. Figures 4(c) and 4(d) show the raw data obtained for different neutron polarizations at the AF wave vectors $Q = (1,0,0.5)$ and $(1,0,1.5)$, respectively, across the AF ordered, paramagnetic orthorhombic and tetragonal phases. In the low-temperature AF ordered state ($T = 2$ K), we find $\sigma_{x}^{SF} \approx \sigma_{y}^{SF}$ consistent with data in Fig. 3(a). On warming to the paramagnetic orthorhombic state [$T_N \leq T < T_s$], temperatures between the solid and dashed vertical lines in Figs. 4(c)-(f)], we have $\sigma_{x}^{SF} > \sigma_{y}^{SF} > \sigma_{z}^{SF}$. This means anisotropic spin excitations at $Q = (1,0,0.5)$ with $M_y - M_z = 0.14M_a + 0.86M_c - M_b > 0$ [Fig. 1(c)]. Finally, on warming to temperatures above $T_s$ [Figs. 4(c) and 4(d)], spin excitations satisfy $\sigma_{x}^{SF} > \sigma_{y}^{SF} \approx \sigma_{z}^{SF}$ and are consistent with data in Figs. 4(a) and 4(b). Therefore, spin excitations in the paramagnetic tetragonal state of NaFeAs are more isotropic with $M_y - M_z = 0.14M_a + 0.86M_c - M_b \approx 0$.

Given the experimental evidence for anisotropic spin excitations in the paramagnetic orthorhombic phase of NaFeAs, it is important to determine its anisotropy along the crystallographic axes. In the AF ordered state, the low-energy spin waves from the two 90$^\circ$ rotated twin domains are centered around wave vectors $Q_{AF} = (\pm 1,0)$ and $(0,\pm 1)$, respectively, in reciprocal space. Therefore,
low-energy spin waves from the \((\pm 1, 0)\) domain are not mixed with those from the \((0, \pm 1)\) domain. However, in the paramagnetic orthorhombic state, spin excitations at the wave vector \((\pm 1, 0)\) may be mixed with paramagnetic excitations from the domain associated with \((0, \pm 1)\), thus complicating the neutron polarization analysis. The key question is whether there are strong paramagnetic scattering at the wave vector \((0, \pm 1)\) in a completely detwinned sample associated with the AF wave vectors \((\pm 1, 0)\). Although such measurement for NaFeAs is unavailable, we note that neutron scattering experiments on a nearly 100% mechanically detwinned BaFe\(_2\)As\(_2\) reveal that spin excitations in the paramagnetic tetragonal state are still centered mostly at \(Q_{AF} = (\pm 1, 0)\) \(\sim 20\) K above the AF and structural transition temperatures\(^{31}\). Therefore, spin excitations of NaFeAs at the wave vectors \(Q_{AF} = (\pm 1, 0)\) may also have little contribution from those associated with the \((0, \pm 1)\) domain in the paramagnetic orthorhombic state. Assuming this is indeed the case, we can carry out neutron polarization analysis in the paramagnetic orthorhombic phase similar to the AF ordered state. Figure 4(e) shows the temperature dependence of \(0.14M_a + 0.86M_c - M_b\) for \(Q = (1, 0, 0.5)\) and \(E = 6\) meV. The data show a clear kink at \(T_N\) and positive scattering below \(T_N\), meaning \(M_b < 0.14M_a + 0.86M_c\). The temperature dependence of \(M_a, M_b,\) and \(M_c\) shown in Fig. 4(f) are determined from combining the data in Figs. 4(a)-(4(d)). Inspection of the Figure reveals clear in-plane magnetic anisotropy with \(M_c > M_b\) in the paramagnetic orthorhombic phase which becomes much smaller in the paramagnetic tetragonal phase [Fig. 4(f)].

Our results suggest that whereas \(M_b, M_c\) evolve smoothly across \(T_N\), \(M_a\) peaks around \(T_N\) indicating divergent longitudinally polarized critical magnetic fluctuations. Both \(\sigma_x^{SF}\) and unpolarized neutron scattering measures \(M_y + M_z\), which is \(0.14M_a + 0.86M_c + M_b\) for \(Q = (1, 0, 0.5)\) and \(0.59M_a + 0.41M_c + M_b\) for \(Q = (1, 0.1, 1.5)\). If \(M_a\) dominates the critical fluctuations near \(T_N\), one would expect a stronger peak due to critical fluctuations at \((1, 0, 1.5)\) than at \((1, 0, 0.5)\) since magnetic structural factor is larger at \((1, 0, 1.5)\)\(^{32}\). Comparison of our data measured at these two wave vectors [Fig. 4(c)-(d)] and unpolarized neutron scattering results in Ref.\(^{32}\) suggest this is indeed the case. For a classical Heisenberg magnetic system with an Ising anisotropy term, one would expect diverging longitudinally polarized spin excitations at \(T_N\) consistent with our observations\(^{36}\).

In previous polarized measurements on parent compound BaFe\(_2\)As\(_2\)\(^{32}\), it was found that the in-plane polarized spin waves exhibit a larger gap than the c-axis polarized ones. However, the spin anisotropy immediately disappears in the paramagnetic tetragonal state above \(T_N\) and \(T_{AF}\)\(^{32}\). In addition, while \(\sigma_x^{SF} - \sigma_y^{SF} \propto M_b\) diverges at \(T_N\), \(\sigma_x^{SF} - \sigma_y^{SF} \propto (\sin^2 \theta M_a + \cos^2 \theta M_c)\) peaks at a temperature slightly below \(T_{AF}\)\(^{32}\). This is different from the results in Fig. 4. Since \(T_N\) and \(T_{AF}\) occur at almost the same temperature in BaFe\(_2\)As\(_2\)\(^{34,36}\), it is unclear whether the system also has magnetic anisotropy in the paramagnetic orthorhombic phase. The discovery of an in-plane spin excitation anisotropy in the paramagnetic orthorhombic phase of NaFeAs suggests the presence of a strong spin-orbit coupling in such a state\(^{31,34-42,44}\). However, we cannot distinguish if such anisotropy is a sole manifestation of spin nematicity or a consequence of the orbital ordering\(^{22,26}\). In a recent X-ray diffraction experiment under pulsed magnetic fields, in-plane field-induced static susceptibility anisotropy with \(\chi_0 > \chi_a\) in the AF ordered state is found to extend to the paramagnetic orthorhombic phase of electron-underdoped Ba\(_2\)(Fe\(_{1-x}\)Co\(_x\))\(_2\)As\(_2\)\(^{28}\). This is 90° rotated from the in-plane dynamic susceptibility anisotropy \((M_a > M_b\) or \(\chi'_a > \chi'_b)\) in the paramagnetic orthorhombic state of NaFeAs. While the static susceptibility anisotropy remains unchanged from the AF ordered phase to the paramagnetic orthorhombic phase in Ba\(_2\)(Fe\(_{1-x}\)Co\(_x\))\(_2\)As\(_2\)\(^{28}\), there is a dramatic switch over of the spin excitation anisotropy across \(T_N\) in NaFeAs, changing from the entirely c-axis polarized spin waves \((M_c \gg M_a \approx M_b \approx 0)\) in the AF ordered phase to \(M_a \geq M_c > M_b\) in the paramagnetic orthorhombic state. Finally, the spin anisotropy becomes much smaller in the paramagnetic tetragonal phase. We note that the static in-plane susceptibility anisotropy observed in transport\(^{22}\) and X-ray diffraction experiments\(^{32}\) occurs at the zero wave vector, while the dynamic susceptibility anisotropy in NaFeAs is at the AF wave vectors \(Q_{AF} = (\pm 1, 0)\).

III. DISCUSSION AND CONCLUSIONS

To qualitatively understand these results, we note that the orthorhombic lattice distortion below \(T_s\) lifts the degeneracy between Fe \(d_{xz}\) and \(d_{yz}\) orbitals and leads to a ferro-orbital order with more doubly-occupied Fe \(d_{xz}\) orbitals and more singly-occupied Fe \(d_{yz}\) orbitals\(^{32}\). In the case of NaFeAs, the Fermi surfaces evolve dramatically from the paramagnetic tetragonal state to the AF ordered state and the splitting of the \(d_{xz}\) and \(d_{yz}\) orbitals starts to occur at a temperature above \(T_{AF}\)\(^{12}\). The angular momentum of \(d_{yz}\) orbitals lies along the \(a\)-axis direction, which pins the ordering spin moment along the \(a\)-axis via spin-orbit interaction. This is indeed observed experimentally as shown in Fig. 1(a)\(^{32}\). Although the electronic structure undergoes an orbital-dependent reconstruction in the nematic state above \(T_s\), primarily involving the splitting of \(d_{xz}\) and \(d_{yz}\)-dominated bands, the splitting mostly occurs in the temperature range above \(T_N\), and there are only small changes across \(T_{AF}\). This is different from the temperature dependent spin dynamic susceptibility across \(T_N\) [Fig. 4(f)], but consistent with the notion that ferro-orbital ordering involving \(d_{xz}\)- and \(d_{yz}\)-bands plays a minor role\(^{12}\). Therefore, it is more likely the observed dynamic susceptibility anisotropy is a manifestation of dynamic spin nematicity coupled with orbital ordering. For a typical
second order AF phase transition, critical spin fluctuations should exhibit a peak at $T_N$. From Fig. 4(f), we see that spin excitations in NaFeAs are dominated by the longitudinal fluctuations ($M_a$ or $N_a^0$) near $T_N$, consistent with diverging longitudinally polarized spin excitations in a Heisenberg antiferromagnet with Ising spin anisotropy. Given the small lattice distortion in the paramagnetic orthorhombic phase of NaFeAs, it is unlikely such an anisotropy term could arise from the lattice distortion. This is consistent with the fact that similar in-plane spin excitation anisotropy has also been observed in the paramagnetic tetragonal phase of superconducting BaFe$_{1.904}$Ni$_{0.096}$As$_2$. Instead, the observed in-plane spin excitation anisotropy is more likely to arise from orbital ordering or anisotropic exchange interactions due to spin nematicity.

In summary, we have discovered that low-energy spin waves in NaFeAs are entirely $c$-axis polarized for energies below $\sim 10$ meV. On warming the system across $T_N$ to the paramagnetic orthorhombic state, a clear in-plane anisotropy develops in the low-energy spin excitations spectra, resulting $M_a \geq M_c > M_b$. Finally, spin excitations become essentially isotropic in the paramagnetic tetragonal phase above $T_N$. These results indicate that the spin excitation anisotropy in superconducting iron pnictides originates from similar anisotropy already present in their parent compounds, and suggest the presence of a spin nematic phase in the paramagnetic orthorhombic state of NaFeAs.

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Using time-of-flight neutron spectroscopy, we have collected spin wave data on NaFeAs throughout the entire Brillouin in the AF ordered state. Based on Heisenberg Hamiltonian fits to the high-energy spin waves, we determine effective magnetic exchange couplings along different crystallographic directions.