On Neutron Star Mergers as the Source of $r$-process-enhanced Metal-poor Stars in the Milky Way

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Abstract

We model the history of Galactic $r$-process enrichment using high-redshift, high-resolution zoom cosmological simulations of a Milky Way–type halo. We assume that all $r$-process sources are neutron star mergers (NSMs) with a power-law delay time distribution. We model the time to mix pollutants at subgrid scales, which allows us to better compute the properties of metal-poor (MP) and carbon-enhanced metal-poor (CEMP) stars, along with statistics of their $r$-process-enhanced subclasses. Our simulations underpredict the cumulative ratios of $r$-process enriched MP and CEMP stars (MP-$r$, CEMP-$r$) over MP and CEMP stars by about one order of magnitude, even when the minimum coalescence time of the double neutron stars (DNSs), $t_{\text{min}}$, is set to 1 Myr. No $r$-process-enhanced stars form if $t_{\text{min}} = 100$ Myr. Our results show that even when we adopt the $r$-process yield estimates observed in GW170817, NSMs by themselves can only explain the observed frequency of $r$-process-enhanced stars if the birth rate of DNSs per unit mass of stars is boosted to $\approx 10^{-4} M_\odot^{-1}$.

Key words: Galaxy: abundances – stars: neutron $r$ stars in the MW’s halo (Barklem et al. 2005; Abate et al. 2016).

In fact, the very existence of CEMP-$r$ stars poses new challenges for the origin of $r$-process elements in the early universe. These stars are believed to form at high redshifts and in low-mass halos where Population III stars have polluted the halo with their carbon-rich ejecta. In such low-mass halos, for a CEMP-$r$ star to form, an $r$-process source that acts on a timescale similar to Population III stars (i.e., $\approx 10$ Myr) is needed (Ramirez-Ruiz et al. 2015).

Could the observed statistics of different classes of $r$-process-enhanced stars be explained by NSMs as the sole source of $r$-process in the early universe? In this study, we address this question by carrying out a set of zoom cosmological simulations of an MW-type halo and modeling NSMs as the sources of the $r$-process material. We improve on crucial aspects of previous such simulations on three fronts: (i) modeling the coalescence timescales of double neutron stars (DNSs) as drawn from distributions motivated by population synthesis analyses (Fryer et al. 1998; Dominik et al. 2012; Behroozi et al. 2014); (ii) identifying Population III stars by following the evolution of pristine gas in each simulation cell with a subgrid model of turbulent mixing that is crucial for properly identifying Population III stars, whose ejecta are the precursor to the formation of CEMP stars (Sarmento et al. 2017; Naiman et al. 2018); and (iii) adopting a high dark matter (DM) particle mass resolution in order to resolve halos where the MP and CEMP stars form in the early universe.

The structure of this work is as follows. In Section 2 we describe our method in detail. In Section 3 we present our results and compare them to observations of MW halo stars. In Section 4 we discuss our results and conclusions. Throughout this paper, we adopt the Planck 2015 cosmological parameters (Planck Collaboration et al. 2016), where $\Omega_M = 0.308$, $\Omega_{\Lambda} = 0.692$, and $\Omega_b = 0.048$ are total matter, vacuum, and baryonic densities, respectively, in units of the critical density $\rho_c$, $h = 0.678$ is the Hubble constant in units of 100 km s$^{-1}$ Mpc$^{-1}$, $\sigma_8 = 0.82$ is the variance of linear...
fluctuations on the $8 \, h^{-1} \, \text{Mpc}$ scale, $n_e = 0.968$ is the tilt of the primordial power spectrum, and $Y\text{He} = 0.24$ is the primordial helium fraction.

2. Method

We used RAMSES (Teyssier 2002), a cosmological adaptive mesh refinement code, which implements an unsplit second-order Godunov scheme for solving the Euler equations. RAMSES variables are cell centered and interpolated to the cell faces for flux calculations; these are then used by a Harten–Lax–van Leer-Contact Riemann solver (Toro et al. 1994).

We performed a set of zoom cosmological simulations of an MW-type halo in order to address whether NSMs can be considered the primary source of r-process enrichment in the early universe. We adopted three different minimum timescales for the coalescence of the DNSs: $\tau_{\text{min}} = 1$, 10, and 100 Myr. We also adopted three different energies for the NS merger event and run simulations: $E_{\text{NSM}} = 10^{50}$, $10^{51}$, and $10^{52}$ erg. In all cases, we stopped the simulations at $z \approx 8.9$ when reionization is complete and the formation of the MP stars largely diminishes. The statistics of different classes of stars displaying a high abundance of r-process elements are then compared against MW’s halo stars.

2.1. Simulation Setup and MW Initial Conditions (ICs)

To initialize our simulations, we first ran a DM-only simulation down to redshift zero in a periodic box with a comoving size of 50 Mpc $h^{-1}$. ICs were generated from MUSIC (Hahn & Abel 2011) for a Planck 2015 cosmology. The virial mass and radius of the halos are derived from the HOP halo finder (Eisenstein & Hut 1998). We used a halo mass cut of $(1.2) \times 10^{12} \, M_{\odot}$ to ensure that we only identified halos with a mass similar to the MW. We found 275 such halos within the desired mass range in our simulation box. We further refined our MW-type halo candidates by requiring them to be isolated systems. We estimated this based on the tidal isolation parameter ($\tau_{\text{iso}}$) approach (Grand et al. 2017). The isolation parameter for each halo is computed as

$$\tau_{\text{iso},i} = M_{200,i}/M_{200} \times (R_{200}/r_1)^{3},$$

where $M_{200}$ and $R_{200}$ are the virial mass and radius of the halo of interest, respectively, and $M_{200,i}$ and $r_1$ are the virial mass of and distance to the $i$th halo in the simulation, respectively. We computed $\tau_{\text{iso,max}}$ for all halos with masses in the range of $(1.2) \times 10^{12} \, M_{\odot}$, by searching within a distance of 10 Mpc $h^{-1}$ centered on the location of each halo. The most isolated halos, i.e., those with the lowest values of $\tau_{\text{iso,max}}$, are our candidate MW-like halos.

Next, we traced the DM particles within $2 \times R_{200}$ for the top five candidates with the lowest values for $\tau_{\text{iso,max}}$ back to the starting redshift. The locations of these DM particles determine the Lagrangian enclosing box. The halo with the smallest box, now our zoom region, was chosen for our simulations to reduce the computational costs.

For the full hydrodynamic simulations, this zoom region is refined to a base level of 12 and 13 for two different sets of simulations corresponding to a DM particle mass of $m_{\text{DM}} \approx 1.2 \times 10^5 \, M_{\odot}$, and $1.4 \times 10^5 \, M_{\odot}$, respectively. The zoom region has sides $4.4 \times 4.2 \times 6.4$ comoving Mpc $h^{-1}$.

2.2. Star Formation and Feedback

The stellar particle mass in the simulation is $m_s = \rho_{\text{th}} \Delta x_{\text{min}}^3 N$, where $\Delta x_{\text{min}}$ is the best resolution cell size achievable and $N$ is drawn from a Poisson distribution

$$P(N) = \frac{N^N \exp(-N)}{N!},$$

where

$$\bar{N} = \frac{\rho \Delta x^3}{\rho_{\text{th}} \Delta x_{\text{min}}^3 \epsilon_\text{e}},$$

and the star formation efficiency $\epsilon_\text{e}$ was set to 0.01 (Krumholz & Tan 2007) in our simulations. Setting $L_{\text{max}}$, the maximum refinement in the simulation, to 24, together with $n_s = 17 \, \text{H cm}^{-3}$ as the threshold for star formation in the cells, results in a stellar particle mass of $\approx 50 \, M_{\odot}$. This is massive enough to host the two supernovae (SNe) needed to create a DNS. $L_{\text{max}}$ is the maximum refinement level in the simulation. A further limitation on star particle formulation is that no more than 90% of the cell’s gas mass can be converted into stars.

In this study, we only modeled r-process element production by NSMs, and slow s-process channels were not modeled. Consequently, we did not model elements such as barium that have both r-process and s-process origin. Also, we did not model Type Ia SNe because of their long average delay times of the order of 200–500 Myr (Raskin et al. 2009). Given the stellar particle mass ($\approx 50 \, M_{\odot}$), 50% of all such particles were assumed to host one core-collapse SN (CCSN), assigned stochastically. Therefore, half of the stellar particles generated a CCSN ejecting a total mass of $m_{\text{sn}} = 10 \, M_{\odot}$, with a kinetic energy of $E_{\text{SN}} = 10^{51}$ erg 10 Myr after the star was formed. The metallicity yield for each CCSN is set to $[Z_{\text{SN}}] = 0.1$, meaning that 1 $M_{\odot}$ of metals is ejected in each CCSN event.

For each newly formed star particle, the ejected mass and energy were deposited into all cells whose centers are within 20 pc of the particle, and if the size of the cell containing the particle is greater than 20 pc, the energy and ejecta are deposed into the adjacent cells (Dubois & Teyssier 2008). Here the total mass of the ejecta is that of the stellar material plus an amount of the gas within the cell hosting the star particle (entrained gas) such that $m_{\text{ej}} = m_{\text{sn}} + m_{\text{ent}} \approx \min(10 \, m_{\text{sn}}, 0.25 \rho_{\text{cell}} \Delta x^3)$. Similarly, the mass in metals added to the simulation is taken to be 15% of the SN ejecta plus the metals in the entrained material, $Z_{\text{e}} = m_{\text{ent}} Z + 0.15 \, m_{\text{sn}} Z_{\text{SN}}$.

We separately tracked the metals generated by Population III stars. These are dubbed “primordial metals,” and their mass is taken to be $Z_{\text{p},\text{e}} = m_{\text{gals}} Z_{\text{p}} + 0.15 \, m_{\text{sn}} Z_{\text{SN}}$. Since the scalar $P_{\text{c}}$ captures the mass fraction of the star particle that represents Population III stars. SN feedback is the dominant driver of turbulence in our simulation, and we have modeled the feedback to be purely in kinetic form. Lastly, we note that we do not model black hole formation and its feedback because its impact is expected to be negligible at this redshift (Scannapieco & Oh 2004; Scannapieco et al. 2005; Croton et al. 2006; Sijacki et al. 2007).

2.3. Cooling

We used CLOUDY (Ferland et al. 1998) to model cooling at temperatures $\gtrsim 10^4 \, \text{K}$. Below this temperature we used Rosen...
was then updated every where (Martin et al. 1996). We computed the cooling rate for each simulation cell based on its density, temperature, and H2 fraction, \( f_{H_2} \). We set the primordial H2 fraction according to Reed et al. (2005) with \( f_{H_2} = 10^{-6} \).

Although we did not explicitly model radiative transfer, we modeled the Lyman–Werner flux from our star particles since these photons destroy H2. We used \( \eta_{H_2} = 10^7 \) photons per stellar baryon (Greif & Bromm 2006) and assumed optically thin gas throughout the simulation volume. The total number of stellar baryons, \( N_{\ast,b} \), was computed each step by totaling the mass in star particles assuming a near-primordial composition \((X = 0.73, Y = 0.25)\). The value of \( f_{H_2} \) was then updated every simulation step:

\[
f_{H_2,\text{new}} = \frac{(f_{H_2,\text{old}} N_{\text{gas}} - N_{\text{LW}})}{N_{\text{gas}}},
\]

(4)

where

\[
N_{\text{LW}} = N_{\ast,b} \eta_{H_2}.
\]

We did not model the formation of H2 since subsequent cooling is dominated by metals shortly after the first stars are formed. Lastly, we included a UV background model based on the Haardt & Madau (1996) model.

2.4. Turbulent Mixing

We made use of the work described in Sarmento et al. (2017) to generate and track new metallicity-related quantities for both the gas and star particles. Specifically, for each cell in the simulation we tracked the average primordial metallicity, \( Z_P \), which tracks the mass fraction of metals generated by Population III stars, and the pristine gas mass fraction, \( P \), which models the fraction of unpolluted gas within each simulation cell with \( Z < Z_{\text{crit}} \). We briefly describe these scalars here, and a more thorough discussion is presented in Sarmento et al. (2017).

The primordial metallicity scalar, \( Z_P \), tracked the metallicity arising from Population III stars. This scalar allowed us to track the fraction of Population III SN ejecta in subsequent stellar populations. Yields from Population III stars are likely to have nonsolar elemental abundance ratios (Heger & Woosley 2002; Umeda & Nomoto 2003; Ishigaki et al. 2014) and contribute to the unusual abundances patterns seen in the halo and UFD CEMP stars. Knowing both \( Z_P \) and the overall metallicity of the gas, \( Z \), allowed us to estimate the abundances of various elements, without having to track each one individually. Similarly, the elemental abundance pattern for regular metals is accounted for by a single scalar \( Z \). By tracking these values for each star particle in the simulations and convolving them in post-processing, we can explore the composition of our star particles through cosmic time, by using a variety of yield models for both Population III and Population II SNe.

Our pristine mass fraction scalar, \( P \), modeled the mass fraction of gas with \( Z < Z_{\text{crit}} \) in each simulation cell. Star formation took place at much smaller scales than the best resolution of typical cosmological simulations. Modeling \( P \) allowed us to follow the process of metal mixing at subgrid scales by quantifying the amount of pristine gas within each cell as a function of time.

Most simulations instantaneously update cells’ average metallicity once they are contaminated with SN ejecta. However, mixing pollutants typically takes several Eddy turnover times (Pan & Scannapieco 2010; Pan et al. 2013; Ritter et al. 2015). By tracking the evolution of \( P \), we can model the formation of Population III stars in areas of the simulation that would normally be considered polluted above \( Z_{\text{crit}} \) in effect increasing the chemical resolution of the simulation. Our model for the pristine fraction is based on accepted theoretical models (Pan & Scannapieco 2010) and has been calibrated against numerical simulations that model the dynamical time required to mix pollutants, due to SN stirring, in an astrophysical context (Pan et al. 2013).

As stellar particles are formed within a cell, they inherit \( Z \), \( P \), and \( Z_p \) from the gas. This allowed us to calculate the fraction of stellar mass in a given star particle that represents metal-free stars, \( P_{\text{sf}} \), as well as the relative contributions that metals from Population III and Population II stars make to the stars that are enriched, \( Z_{\text{sf}}/Z_{\text{p}} \).

The ejecta compositions for Population II and Population III stars are indicated in Table 1. Properly accounting for turbulent mixing enables us to identify the Population III stars whose stellar yields (carbon-rich ejecta) are different from those of Population II stars and are responsible for the formation of CEMP stars. We express the abundance ratios of a star compared to that of the Sun as

\[
[A/B]_\star = \log\left( \frac{N_A}{N_B} \right)_\star - \log\left( \frac{N_A}{N_B} \right)_\odot.
\]

(6)

The solar abundance of Eu (log \( \epsilon_{\text{Eu}} \)) is assumed to be 0.52 (Asplund et al. 2009) in the notation of log \( \epsilon_X = \log(N_X/N_H) + 12 \), where \( N_X \) and \( N_H \) are the number densities of element X and hydrogen, respectively. Likewise, for carbon we adopt log \( \epsilon_C = 8.43 \) and for iron log \( \epsilon_{\text{Fe}} = 7.5 \).

We note that subgrid turbulent mixing is only modeled for the metals and not the r-process ejecta. However, due to the high resolution of these simulations, we observe a negligible difference in metal enrichment due to the computation of subgrid turbulent mixing. Therefore, we assume that the same holds for r-process material, as it is treated as another scalar field similar to the metals in the code.

2.5. Modeling NSMs

We have modeled the formation of DNSs to take place for a tiny fraction \((10^{-3})\) of stellar particles chosen to go SNe. This corresponds to one DNS per \(10^7 M_\odot\) of stars, which translates into an NSM rate of \(\approx 10^{-4} \text{yr}^{-1}\) at \( z = 0 \) (van de Voort et al. 2015).

| Element | \( X/Z \) 1 Gyr | \( X/Z_p \) 60 \( M_\odot \) Population III SNe |
|---------|----------------|-----------------------------------|
| C       | \( 1.68 \times 10^{-1} \) | \( 7.11 \times 10^{-1} \) |
| Fe      | \( 5.39 \times 10^{-2} \) | \( 2.64 \times 10^{-12} \) |

Note. The mass fractions of metals for selected elements used to model the normal and primordial metallicity of star particles in our simulation.

Table 1: Mass Fractions of Metals
The simulation with minimum time for merging of 1 Myr is named T100E51. All three simulations have a DM particle mass of $1.2 \times 10^5 M_\odot$. The second column indicates the minimum timescale for merging of the DNSs in a power-law distribution, the third column corresponds to the energy of the NSM event, and the fourth column is the stopping redshift of the simulation.

The particle chosen to host a DNS first undergoes two CCSN explosions, corresponding to the two progenitor stars. Afterwards, the particle was assigned a delay time distribution drawn from a power law $t_{\text{merge}} \propto t^{-1}$ (e.g., Dominik et al. 2012; Mennekens & Vanbeveren 2016) with a minimum of $t_{\text{min}} = 1$, 10, or 100 Myr (for three separate simulations) and maximum of $t_{\text{max}} = 10$ Gyr, respectively. Note that this time is after the formation of the second neutron star in the binary. Once the merger time elapsed, we simulated the generation of $r$-process elements via a third explosion with $E_{\text{NSM}} = 10^{51}$ erg in our fiducial run, while we explored $E_{\text{NSM}} = 10^{50}$ and $10^{52}$ erg cases separately.

### 2.5.1. Europium Yield

We set the fiducial value of the europium yield in the NSM events in our simulations based on the NS–NS merger detected by aLIGO/Virgo (GW170817). We adopted the estimated Eu yield of $1.5 \times 10^{-5} M_\odot$ for each NS merger event in our simulation. This number reflects the lanthanide-rich material ejected in the post-merger accretion disk outflow in an NS–NS merger event with the maximum value of 0.04 $M_\odot$ (Cowperthwaite et al. 2017) multiplied by the abundance pattern of the solar $r$-process residuals (Côté et al. 2018b). The disk wind ejecta could be lanthanide-rich depending on the lifetime of the hypermassive neutron star prior to collapsing into a black hole (Metzger & Fernández 2014; Siegel & Metzger 2017). We adopted this value since, in order to answer the question whether NSMs could by themselves explain the statistics of the $r$-process-enhanced stars in the MW’s halo, one needs to be conservative in the assigned yields.

### 2.6. Simulation Parameterizations

We carried out five different simulations in this paper. We name the simulations as T$x$E$y$, where $x$ stands for the minimum time for coalescence of the NSMs and $y$ stands for the energy for the NSM event in cgs units. For example, T10E51 stands for the simulation with minimum time for merging of the NSMs set to 10 Myr with $E_{\text{NSM}} = 10^{51}$ erg. The DM particle mass resolution is $m_p \approx 1.2 \times 10^5 M_\odot$, and our stellar particle mass is fixed to be 50 $M_\odot$. We stopped the simulation at $z \approx 8$. All five simulations are summarized in Table 2.

### 3. Results

We start by showing the overall star formation history of our MW-type galaxy and its corresponding metallicity evolution. The top panel of Figure 1 shows the comoving star formation rate density (SFRD) of the T1E51 simulation that we ran down to redshift $z = 8.2$. The cyclic SFR trend with an overall increase toward lower redshift is characteristic of all simulations, while the exact level of the SFR can vary depending on the overdensity, which is resimulated at higher resolution (Xu et al. 2016). The improved DM mass resolution in the Renaissance simulation allows it to track star formation in

| Simulation | $t_{\text{max}}$ (Myr) | $E_{\text{NSM}}$ (erg) | $z_{\text{min}}$ |
|------------|-------------------------|------------------------|-----------------|
| T1E51      | 1                       | $10^{51}$              | 8.2             |
| T10E50     | 10                      | $10^{50}$              | 8.9             |
| T10E51     | 10                      | $10^{51}$              | 8.9             |
| T10E52     | 10                      | $10^{52}$              | 8.9             |
| T100E51    | 100                     | $10^{51}$              | 8.9             |

**Table 2** Simulation Parameters

Note. The characteristics of the simulations presented in this paper. We adopt the notation of T$x$E$y$ to name each simulation, where $x$ stands for the minimum time for coalescence of the NSMs and $y$ stands for the energy for the NSM event in cgs units. The simulation with minimum time for merging of 1 Myr and $E_{\text{NSM}} = 10^{51}$ erg is named T1E51. The simulation with minimum time for merging of the binaries set to 100 Myr is named T100E51. All three simulations have a DM particle mass of $1.2 \times 10^5 M_\odot$. The second column indicates the minimum timescale for merging of the DNSs in a power-law distribution, the third column corresponds to the energy of the NSM event, and the fourth column is the stopping redshift of the simulation.
smaller overdensities at earlier times. Hence, we see a higher SFRD at early times for the normal case as compared to simulations with lower DM mass resolution. The Renaissance simulation has a comoving resolution of 19 pc as compared to simulations with lower DM mass resolution. The MDF for stars grouped based on their formation redshift. The MDF for stars formed at \( z > 14 \) is shown in blue, and the MDF for those formed at \( z > 8.2 \) is shown in black. As expected, the overall metallicity increases with time, while the rate of change of the MDF slows down toward lower redshifts. These are all the stars in the simulation, not categorized per halo mass.

Figure 2 shows rendered images of the DM, hydrogen, \( r \)-process, and metal distribution at \( z = 8.95 \). The metals are produced by the CCSN and the \( r \)-process by the NSM, which follow a power-law delay time distribution with a minimum time for merging of 10 Myr. When comparing the metal and \( r \)-process distribution, we see that the delay in NSMs caused some halos to be enriched with metals but no \( r \)-process material.

3.1. Formation of CEMP Stars

Modern surveys of the Galactic halo, as well as UFDs, indicate that CEMP stars (defined as those with \([C/Fe] > 1\) and \([Fe/H] < -1\)) become more prevalent as overall metallicity decreases (Beers & Christlieb 2005). In fact, these surveys indicate that the fraction of CEMP stars is as high as 25% for stars with \([Fe/H] < -2.0\) (Komiya et al. 2007) and possibly as high as 40% for stars with \([Fe/H] < -3.5\) (Lucatello et al. 2006). Hansen et al. (2016) found that only about 17% ± 9% of all the CEMP-no stars (which display no enhancement to \( s \) — or \( r \)-process elements) exhibit binary orbits. Therefore, the dominant formation scenario of the CEMP stars is not through the mass transfer from a binary companion. The discovery of damped Ly\( \alpha \) systems with enhanced carbon (Cooke et al. 2011, 2012) suggests that these stars are born in halos that are pre-enriched by carbon (Sharma et al. 2018).

The left panel of Figure 3 shows the distribution of the stars in the \([C/Fe]—[Fe/H]\) plane. Each point is a star particle color-coded given its age (i.e., red shows the stars that formed at the highest redshift in the simulation). The adopted Fe and C yields from Population II and Population III SNe are listed in Table 1. Each star formation event traces a line with a negative slope in this plane. The oldest stars trace a line with more negative slope compared to the younger stars formed in the simulation. Since carbon is primarily generated from Population III stars and Population III stars are formed in MP regions, naturally we see higher carbon enrichment toward lower metallicities. This is consistent with the observations of the CEMP stars, where a higher percentage of the stars show \([C/Fe] > 1\) toward lower metallicities. The location of the stars in the \([C/Fe]—[Fe/H]\) plane that defines a CEMP star is outlined with a dashed blue line.

The right panel of Figure 3 shows the cumulative fraction of the MP stars that are CEMPs as a function of redshift. The black star indicates the observed cumulative ratio of \( \approx 5\% \) (Lee et al. 2013), which is based on the Sloan Digital Sky Survey (SDSS)/SEGUE data and consistent with other groups (Frembel et al. 2006; Carollo et al. 2011; Placco et al. 2014). The orange hexagon is the updated analysis from Yoon et al. (2018). We note that in this plot we have adopted \([C/Fe] > 0.7\) for the
yields from Population II and Population III SNe are listed in Table 1. The Eu yield per NS merger event is set to 1.5

The middle panel of Figure 4 shows the distribution of the stars in the T10E51 simulation at \( z \approx 8.9 \) in the [Eu/H]--[Fe/H] (left panel), [C/Fe]--[Fe/H] (middle panel), and [C/Fe]--[Eu/Fe] planes (right panel). Each point is a star particle color-coded given its age (i.e., red shows the stars that formed at the highest redshift in the simulation). The adopted Fe and C yields from Population II and Population III SNe are listed in Table 1. The Eu yield per NS merger event is set to \( 1.5 \times 10^{-5} M_\odot \) based on the yield estimates from NS–NS mergers detected by aLIGO/Virgo (GW170817). This reflects the lanthanide-rich material ejected in the wind ejecta from an NS–NS merger event. In the middle panel, we also show the five stars in Reticulum II whose abundances in both carbon and europium are measured.

3.2. Formation of MP r-process Stars

Figure 4 shows the distribution of stars in the [Fe/H]--[Eu/H], [C/Fe]--[Eu/Fe], and [Fe/H]--[Eu/Fe] planes in T10E51 at \( z \approx 9 \). Each data point indicates one star particle in the simulation, and we show a random sample of 20% of all the stars in the simulation box. Each data point is color-coded by the stellar age.

Close inspection of the distribution of stars in the [Fe/H]--[Eu/H] plane shows that star formation events trace lines with different slopes, mostly from linear in the early times to vertical at later cosmic times. A horizontal line indicates a star formation event in a region where the gas has a dispersion in [Fe/H] but europium is well mixed, while the opposite holds for a vertical line as we go to more metal-rich stars. These are on average younger stars that have recently formed in halos enriched by iron. These halos are old enough for the iron to be well mixed; however, a recent NSM event explains the large dispersion along the [Eu/H] axis. The correlation between [Eu/H] and [Fe/H] at high metallicities that are shown by young stars is an imprint of the fact that stars start to form in halos where there has been pre-enrichment by both SNe II and DNSs.

The middle panel of Figure 4 shows the distribution of the stars in the [Eu/Fe]--[C/Fe] plane. One can use the distribution of the stars in this plane to select CEMP-\( r \) stars. Each line traces one star formation event, and as can be seen, the lines have a positive slope, indicating that those stars that are carbon enriched, and therefore born in halos enriched with Population III ejecta, also show higher [Eu/Fe] values. This is because Population III star formation results in both SNe that eject large amounts of carbon into their surroundings and DNSs that are strong sources of europium. This leads to the observed correlation for old stars. As can be seen, older stars are clustered toward the lower end of [C/Fe] and do not show the strong correlation between [Eu/Fe] and [C/Fe] as is seen for the young stars. This is due to the fact that the metal production dominates over that of carbon in more massive halos, and in general as the formation of Population III stars ceases, the new
stars in the halo are born with lower [C/Fe]. In such systems, a single NSM event will lead to large dispersion along the [Eu/Fe] axis, as is observed by how the old stellar particles are clustered toward the lower end of [C/Fe].

In the middle panel, we also show the five stars in the UFD galaxy Reticulum II (Ji et al. 2016) that have measured abundances in both carbon and europium. The fact that there are practically no stars in our simulation that match Ret II abundances in both of these elements potentially shows that the europium yield or NSM merger rate adopted as a fiducial value in our simulations needs to be boosted by a large factor. We return to this point in the next section.

The right panel of Figure 4 shows the distribution of the stellar particles in the [Fe/H]−[Eu/Fe] plane. The location of the stars in this plane is used to define different categories of MP r-process-enhanced stars.

### 3.3. Comparison with Observations of r-process-enhanced MP Stars

MP stars encode a wealth of information about the conditions in the early universe, when these stars were formed (Frebel & Norris 2015). Such stars are divided into two categories, MP-rI and MP-rII, based on the r-process element abundance in their spectra. MP-rI stars are MP stars that show mild enhancement of r-process elements, namely, 0.3 < [Eu/Fe] < 1 and [Fe/H] < −1.5. MP-rII stars are defined as those with higher levels of r-process abundance, namely, 1 < [Eu/Fe] and [Fe/H] < −1.5. These two categories are outlined in the right panel of Figure 4. Based on the Hamburg/ESO r-process Enhanced Star survey (HERES; Barklem et al. 2005), out of 253 MP stars with −3.8 < [Fe/H] < −1.5, about 5% are MP-rII stars and another 15%−20% are MP-rI stars. Separately, based on the SAGA database of stellar abundances, Abate et al. (2016) reported that out of 451 MP stars with Eu and Ba abundance, 26 (~6%) are found to belong to the MP−rII class.

The left panel of Figure 5 shows the cumulative fraction of all the MP stars that are MP-rI. This is cumulative in the sense that it indicates the fraction of all the MP stars formed by redshift z that belong to the MP-rI class. We show the results for T1E50 (solid blue), T1E51 (dashed green), T1E52 (dot-dashed red), and T1E51 (solid black). The T100E51 simulation results in zero MP-rI stars and is not shown in the plots. The black filled circle shows the ratio of MP-rI over MP stars from observations of the MW’s halo stars, which is about 20% (Abate et al. 2016). Our simulations predict that the ratio is more than an order of magnitude below the level observed if the source of r-process is solely NSMs given the adopted rate of their formation and assigned r-process yield.

Our results should be thought of in the context of the imposed delay time distributions. When a minimum timescale of 1 Myr is considered for merging of the DNSs when they are formed, given the power-law distribution, the median merging timescale of the DNSs is about 100 Myr. When the minimum timescale is changed to 0 or 10 Myr, the median timescale for merging changes from 3 to 300 Myr, respectively. These median timescales matter in that they need to be compared to a typical phase of star formation that lasts in a given MW progenitor halo. Longer merging timescales relative to the star formation timescale would lead to an NSM event that does not effectively enrich the medium such that r-process material gets recycled into the stars formed after the event. This is either because the star formation has ceased after the NSM event or because a new phase of star formation occurs with a delay long enough to make the r-process material get too diluted before getting recycled into the new stars. This is clearly shown in the simulation with a minimum merging timescale of 100 Myr, in that no MP-rI stars are born in that simulation.

The middle panel of Figure 5 shows the cumulative fraction of the MP stars that are categorized as MP-rII. The lines are the same as in the left panel. The ratio of MP-rII stars to MP stars predicted in the simulation is about an order of magnitude less than the observed level in the MW halo.

The right panel of Figure 5 shows the cumulative fraction of CEMP-r to all the CEMP stars. CEMP-r stars are defined as a subclass of CEMP stars with [Eu/Fe] > 1 and [Ba/Eu] < 0, and there are a handful of theories regarding their formation (Abate et al. 2016). The location of this category of stars is outlined with dashed brown lines in the middle panel of Figure 4. Out of 56 CEMP stars with barium and europium abundances, Abate et al. (2016) found 5 to be CEMP-r stars and 26 to be CEMP-r/s stars. About a few percent of all the CEMP stars are CEMP-r in our simulation, which is an order
of magnitude less than the observed frequency of this class of stars.

The impact of the $E_{\text{NSM}}$ is understood in that lower energies tend to disperse the $r$-process material in a smaller volume, and therefore the higher concentration of $r$-process leads to the formation of $r$-process-enhanced stars. The impact of the $E_{\text{NSM}}$ is subdominant compared to the effect of the minimum time considered for the delay time distribution. Lower delay times (1 Myr; black line) lead to more NSM events in a halo, while large minimum times (as in the T100E51 simulation) result in formation of no $r$-process-enhanced stars.

In all three panels of Figure 5, the thin black dashed lines indicate an assumed NSM merger rate of $\approx 2 \times 10^{-4} M_{\odot}^{-1}$, or equivalently a europium yield of $3 \times 10^{-4} M_{\odot}$, which matches the statistics of the $r$-process MP stars. This boosted NSM merger rate, however, overpredicts the same statistics for the CEMP stars. The mismatch between what Eu yield is required to match the observations shows either that we need more robust statistical data for the CEMP stars or that the $r$-process MP stars have been enriched by a separate source in addition to the NSMs.

4. Summary and Discussion

While both CCSNe and NSMs could explain the observed abundance of $r$-process elements in the Galaxy (Cowan et al. 1991; Woosley et al. 1994; Rosswog et al. 1999, 2000; Argast et al. 2004; Kuroda et al. 2008; Wanajo 2013; Wehmeyer et al. 2015), only $r$-process production in NSMs has been measured directly, and therefore we model the production of $r$-process through NSMs.

We performed cosmological zoom simulations of an MW-type halo with DM particle mass resolution that can resolve halos of mass $\sim 10^{7} - 10^{8} M_{\odot}$ with spatial resolution of $\sim 5$ pc. These high-resolution zoom simulations are aimed at estimating the observed high frequency of $r$-process-enhanced stars in the MW's halo. We assume that the only $r$-process sources are NSMs that are assigned delay time distribution drawn from a power law, as predicted in population synthesis codes (Dominik et al. 2012). We assign europium yield to the NSM events representative of assuming 0.04 $M_{\odot}$ wind ejecta with solar $r$-process pattern residual possible for GW170817 (Côté et al. 2018b).

We track the formation of MP and CEMP stars and their $r$-process-enriched counterpart MP-rI, MP-rII, and CEMP-r stars, and we study the impact of two parameters in our study: (i) the minimum timescale for merging after a DNS is formed, and (ii) the impact of $E_{\text{NSM}}$ on mixing the $r$-process material in a halo. Our simulations underpredict the observed ratio of $r$-process-enhanced stars to their parent category by about an order of magnitude. We note that implementing the natal kicks would further reduce this enrichment level.

Our findings show that increasing the minimum timescale for merging of the DNSs results in a drop in the overall statistics of the $r$-process-enhanced MP stars. This is due to the fact that a longer minimum timescale for merging of the DNSs leads to lower overall NSM events during a given time span, while increasing the median merging timescale of the DNSs. For example, the median timescale for merging of DNSs is (3, 100, 300) Myr if the minimum timescale is set to (0, 1, 10) Myr, respectively. Similarly, the lower the energy of the NSM event, the less mixing the $r$-process material experiences in the halo, and this actually leads to higher levels of $r$-process enhancement for the subsequent stars formed in the halo. The impact of the assumed $E_{\text{NSM}}$ is subdominant compared to the impact that the merging timescale has on the final level of $r$-process enrichment.

Given that, with increasing the minimum time for merging from 1 to 100 Myr, we are not able to form any MP-rI or CEMP-r stars, fast-merging channels for the DNSs seem to be a requirement to make NSMs contribute modestly to $r$-process enrichment of the Galaxy at high redshifts.

In order to match the observed enrichment, we can think of two options: (i) adopting a higher Eu yield and (ii) increasing the DNS birth rate. Regarding the first option, it is highly unlikely that higher Eu yields are possible from an NSM event. The adopted yield is estimated from GW170817 (Cowperthwaite et al. 2017; Côté et al. 2018b) assuming a disk ejecta of mass 0.04 $M_{\odot}$. However, we note that in Naiman et al. (2018) the adopted yield is three times higher than what we have adopted in our study.

Regarding the second option, there is a large tension between the observed NS merger rates and the rates predicted from population synthesis models (Belczynski et al. 2017; Chrislinska et al. 2018). The value of one merger per $10^{5} M_{\odot}$ of stars adopted in this work corresponds to the MW rate of NSMs of $R_{\text{MW}} \approx 10^{-4} \text{yr}^{-1}$ (van de Voort et al. 2015). This rate is on the assumption that the minimum timescale for merging of the binaries is 30 Myr and the final stellar mass of the MW is about $3 \times 10^{10} M_{\odot}$. This rate corresponds to almost the maximum rate predicted in population synthesis models with various variations, and about an order of magnitude above the observational estimates based on galactic double pulsars (Kim et al. 2015). However, translating this rate into the local rate, we would be similar to the LIGO/Virgo merger rate estimate of $1540 - 13200 \text{ Gpc}^{-3} \text{yr}^{-1}$ (Abbott et al. 2017a).

The NSM birth rate is subject to the details of the models implemented in the population synthesis codes (Belczynski et al. 2002, 2008; Dominik et al. 2012). In the standard model assumed in these models, which is mostly concerned with the assumptions governing the common envelope (CE) phase during the formation of a compact binary system, we find that with the adopted Kroupa initial mass function (Kroupa & Weidner 2003) the DNS birth rate is about 2.5 per $10^{5} M_{\odot}$ of stellar mass modeled. However, this birth rate can be boosted by a factor of three in variation of their standard model (e.g., in variation 15 of Dominik et al. 2012), which translates into NSM birth rates of about 6 times what we have assumed in this study. While increasing the $r$-process yield will not impact the star formation history of our Galaxy and simply will shift the stellar particles up and down in the [Eu/Fe] or [Eu/H] axis, we could not treat birth rates similar to the yields. Higher birth rates will affect the iron yield from the CCSN, as their number density would be affected. In other words, while in our simulation there is one DNS born per 1000 CCSNe, changing that to one DNS per 100 CCSNe will significantly impact the metallicity trends in our halos.

Based on our results, higher yields or higher birth rates with fast-merging timescales are needed to match the observations of the MW halo’s MP $r$-process-enhanced stars. Similar conclusions have been reached based on chemical evolution studies of the Galaxy (Côté et al. 2018a), and it has been suggested that a second source of $r$-process is needed in order to explain the observed trends in the MW’s disk. Moreover, the
long delay between GW170817 and the star formation activity of its host galaxy, NGC 4993 (Levan et al. 2017), indicates that the merger rate at short delay times is different at high redshifts. Whether either of such choices would be consistent with the expected theoretical calculations of the $r$-process yield in NS merger events or the metallicity evolution at highest redshift remains to be explored. Upcoming data from the R-Process Alliance is projected to increase the detected number of MP-rII and MP-rI stars to 125 and over 500, respectively, in the next several years (Hansen et al. 2018; Sakari et al. 2018). Moreover, upcoming data on the frequency of CEMP-$r$ stars from high-resolution observations of a sample of approximately 200 bright CEMP stars by K. C. Rasmussen et al. (2019, in preparation) are likely to provide a much-improved estimate of the frequencies of CEMP subclasses.

5. Future Work

We have not modeled the natal kicks of the DNSs in this work. However, their impact is expected to be significant specifically if natal kicks and delay times are not correlated for a DNS. DNSs are thought to be the precursors of the short gamma-ray bursts (sGRBs), and the location of sGRBs with respect to galaxies in the field can provide clues into the natal kick distribution of the DNSs. By studying hostless GRBs, Fong & Berger (2013) derived natal kick velocities in the range of 20–140 km s$^{-1}$, with a median value around 60 km s$^{-1}$.

From a theoretical perspective, in population synthesis models of DNSs (Fryer et al. 1998), binary systems with different initial masses for each star, initial eccentricity, orbital separation and natal kick velocities are simulated, and the center of mass velocity after the formation of the second NS is studied. Such models arrive at center of mass velocity distribution with an exponential profile and a median of 180 km s$^{-1}$ (Behroozi et al. 2014). Safarzadeh & Côté (2017) studied the impact of DNS's natal kick on the Galactic $r$-process enrichment and concluded that almost 50% of all the NSMs that have occurred in the star formation history of an MW-type system do not contribute to the $r$-process enrichment, as the DNSs merge well outside the galaxy’s effective radius.

For systems with shallow potential wells such as the UFDs (Eisenstein, D. J., & Hut, P. 2011, MNRAS, 416, 997), the $r$-process yield in NSs can be significantly enhanced if natal kicks and delay times are correlated for galaxies in the MW. For that we that would need to model the formation of the AGB stars (Sharma et al. 2018). This work could be expanded to a whole suite of MW-type halos in large simulations such as Auriga (Grand et al. 2017) and the Caterpillar suite of simulations (Griffen et al. 2016) to achieve a reliable halo-to-halo scatter.

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