Stochastic Electron Acceleration by the Whistler Instability in a Growing Magnetic Field

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Abstract

We use 2D particle-in-cell simulations to study the effect of the saturated whistler instability on the viscous heating and nonthermal acceleration of electrons in a shearing, collisionless plasma with a growing magnetic field, $B$. In this setup, an electron pressure anisotropy with $p_{\perp,e} > p_{\parallel,e}$ naturally arises due to the adiabatic invariance of the electron magnetic moment ($p_{\parallel,e}$ and $p_{\perp,e}$ are the pressures parallel and perpendicular to $B$). If the anisotropy is large enough, then the whistler instability arises, efficiently scattering the electrons and limiting $\Delta p_e (\equiv p_{\perp,e} - p_{\parallel,e})$. In this context, $\Delta p_e$ taps into the plasma velocity shear, producing electron heating by the so-called anisotropic viscosity. In our simulations, we permanently drive the growth of $|B|$ by externally imposing a plasma shear, allowing us to self-consistently capture the long-term, saturated whistler instability evolution. We find that besides the viscous heating, the scattering by whistler modes can stochastically accelerate electrons to nonthermal energies. This acceleration is most prominent when initially $\beta_e \rightarrow 1$, gradually decreasing its efficiency for larger values of $\beta_e (\equiv 8\pi p_e / |B|^2)$. If initially $\beta_e \sim 1$, then the final electron energy distribution can be approximately described by a thermal component, plus a power-law tail with a spectral index of $\sim 3.7$. In these cases, the nonthermal tail accounts for $\sim 5\%$ of the electrons and for $\sim 15\%$ of their kinetic energy. We discuss the implications of our results for electron heating and acceleration in low-collisionality astrophysical environments, such as low-luminosity accretion flows.

Key words: acceleration of particles – accretion, accretion disks – instabilities – plasmas

1. Introduction

Nonthermal electrons are usually required to explain observations of various astrophysical systems where MHD turbulence is expected to be present. For example, nonthermal electrons are typically needed to explain the quiescent radio emission in some low-luminosity AGNs (Liu & Wu 2013), as well as in Sgr A*, the supermassive black hole at the center of the Milky Way (Özel et al. 2000; Yuan et al. 2003; Ball et al. 2016). Nonthermal electrons are also necessary to explain the near-infrared (NIR) and X-ray emission from Sgr A* flares (Yuan et al. 2004; Ponti et al. 2017). In the intracluster medium (ICM), the presence of nonthermal electrons is commonly required to explain the extended radio synchrotron emission from some galaxy clusters (see Brunetti & Jones 2014 for a review).

Several physical processes have been proposed to explain electron acceleration in these systems, including: diffusive shock acceleration (see Marcowith et al. 2016 for a review), magnetic reconnection (Sironi & Spitkovsky 2014; Li et al. 2015), and various stochastic (second order Fermi) acceleration processes (Lynn et al. 2014; Zhdankin et al. 2017). In general, the disparity between MHD length-scales and the Larmor radii of particles makes it difficult for MHD turbulence to accelerate electrons via efficient pitch-angle scattering, especially if their energy spectra are initially thermal. Previous works have proposed that this difficulty can be overcome by the resonant scattering provided by whistler waves, producing efficient stochastic electron acceleration in accreting systems (Dermer et al. 1996; Petrosian & Liu 2004). In these works, however, the efficiency of the acceleration depends (among other parameters) on the spectrum of the whistler fluctuations, which is treated as an input of the models. In this work, we use particle-in-cell (PIC) simulations to show that pitch-angle scattering by whistler modes can indeed produce efficient stochastic electron acceleration in the context in which the whistler waves are consistently generated by magnetic field amplification due to a plasma velocity shear.

A key ingredient in our proposed mechanism is electron heating by the so-called anisotropic viscosity. This viscous heating arises due to anisotropic pressure tapping into the energy contained in the plasma velocity shear. For an incompressible, homogeneous plasma with no heat flux, the electron internal energy density, $U_e$, changes at a rate (Kulsrud 1983; Snyder et al. 1997),

$$\frac{\partial U_e}{\partial t} = q\Delta p_e,$$

where $q$ is the growth rate of the magnetic field ($q = dB/dt/B$), with $B = |B|$, and $\Delta p_e = p_{\perp,e} - p_{\parallel,e}$ is the difference between the electron pressure perpendicular and parallel to $B$. In a collisionless plasma, the difference between $p_{\perp,e}$ and $p_{\parallel,e}$ is a consequence of the adiabatic invariance of the electron magnetic moment, $p_e \equiv v^2_{\perp,e}/B$, where $v_{\perp,e}$ is the electron velocity perpendicular to $B$. Thus, magnetic field amplification by plasma shear generically drives $p_{\perp,e} > p_{\parallel,e}$ giving rise to electron heating. This process, however, is expected to be limited mainly by the whistler instability (Gary & Wang 1996), which is triggered when $\Delta p_e$ surpasses an instability threshold, although ion-scale instabilities can also play a role (Riquelme et al. 2016).

In this work, we show that besides controlling the viscous heating of the electrons, the scattering by the whistler waves can accelerate a fraction of the electrons to energies significantly above thermal. For this, we use 2D PIC simulations of a plasma subject to a permanent shear motion, which continuously amplifies the background magnetic field. Given that this shear motion can be caused by the presence of...
of the mean field evolves as $d \langle B_z \rangle / dt = -s B_0$ (throughout this paper, $\langle \rangle$ may represent an average over volume or over particles, depending on the context), implying a net growth of $\langle |B| \rangle$. This, due to $\mu_e$ conservation, drives $p_{\perp,e} > p_{||,e}$ during the whole simulation.

The varying physical parameters between our runs are their initial $\beta_e$ ($\beta_{e,\text{init}}$) and the electron magnetization, which is quantified by the ratio between the initial electron cyclotron frequency and the shear parameter of the plasma, $\omega_{ce}/s$. In our runs, we use electron magnetizations that satisfy $\omega_{ce}/s \gg 1$, but are still much smaller than expected in real astrophysical settings. Because of this, we made sure to reach the regime where $\omega_{ce}/s$ is large enough to not to play any role in our final results.

All of our simulations have initially $k_\parallel T_e/m_e c^2 = 0.28$ ($k_\parallel$, $T_e$, and $m_e$ are the Boltzmann’s constant, the electron temperature, and the electron mass), which implies $\omega_{ce}/\omega_{pe} \approx 0.75/\beta_e^{1/2}$ ($\omega_{pe}$ is the electron plasma frequency). Their numerical parameters are: the number of macro-electrons per cell ($N_{ppc}$), the electron skin depth in terms of grid point spacing ($c/\omega_{pe}\Delta_x$), and the box size in terms of the initial electron Larmor radius ($L/R_{L,e}$)

\[ \text{Table 1} \]

| Simulation | $\omega_{ce}/s$ | $\beta_{e,\text{init}}$ | $c/\omega_{pe}\Delta_x$ | $N_{ppc}$ | $L/R_{L,e}$ |
|------------|----------------|--------------------------|-------------------------|----------|------------|
| S1         | 1200           | 1                        | 15                      | 80       | 110        |
| S2         | 1200           | 2                        | 15                      | 160      | 78         |
| S3         | 3000           | 2                        | 15                      | 160      | 78         |
| S4         | 1200           | 5                        | 10                      | 160      | 74         |
| S5         | 3000           | 5                        | 10                      | 160      | 74         |
| S6         | 1200           | 10                       | 7                       | 160      | 74         |

Note. Simulation parameters: the initial electron magnetization $\omega_{ce}/s$, $\beta_{e,\text{init}}$, the electron skin depth $c/\omega_{pe}\Delta_x$ ($\Delta_x$ is the grid point separation), the number of electrons per cell $N_{ppc}$, and the box size in units of the initial electron Larmor radius $L/R_{L,e}$. In all runs, initially $k_\parallel T_e/m_e c^2 = 0.28$ and $c = 0.225\Delta_x/D_z$, where $D_z$ is the simulation time step.

3. The Physics of Electron Heating by Anisotropic Viscosity

In this section, we describe the process of electron heating by anisotropic viscosity. As a fiducial case, we use simulation S2 of Table 1. Figure 1 shows an example of magnetic and electric field fluctuations at $t \cdot s = 2$, which naturally arise, as we continuously drive the growth of $\langle B \rangle$ (we only show the $z$ components). The black arrows in Figure 1(a) represent the projection of $\langle B \rangle$ on the $x$–$y$ plane, showing that $|\langle B_z \rangle| \approx 2|\langle B_x \rangle|$, which is consistent with magnetic flux freezing, provided that initially $\langle B \rangle = B_0 \hat{x}$. Figure 1 also shows that the field fluctuations are nearly parallel to $\langle B \rangle$ and dominated by wavenumbers $k$ with $kR_{L,e} \sim 0.2$, in which both are

The simulations are performed in the “shearing coordinate system” described in Riquelme et al. (2012), where the shearing velocity of the plasma vanishes, and both of Maxwell’s equations and the Lorentz force on the particles are modified accordingly.

3 As a reference, at $\sim$10 Schwarzschild radii from Sgr A’, the expected conditions in the accreting plasma imply $\omega_{ce}/s \sim 10^3$ (e.g., Ponti et al. 2017), where we have approximated $s$ as the Keplerian rotation period at that radius.

5 Throughout this paper, $R_{L,e}$ will be a time dependent quantity, which coincides with $R_{L,e}^{\text{ini}}$ at $t = 0$ and takes into account the evolution of $\langle |B| \rangle$ and of the rms electron velocity.
features that roughly coincide with the characteristics of marginally stable whistler modes (Gary & Wang 1996; Yoon et al. 2011).6 Figure 2 shows how the time evolution of the whistler instability in our shearing setup determines the pressure anisotropy, as well as the viscous heating of the electrons. First, Figure 2(a) shows how the plasma shears make \((B_z)^2\) (dotted red) grow while \((B_y)^2\) (dotted black) is kept constant (in our runs \((B_z)\) is identically zero). The solid lines show the energy in the fluctuating field \(\delta B\), separated into its component perpendicular \((\delta B_z^2\); green) and parallel \((\delta B_y^2\); blue) to \(\langle B \rangle\). We see that there is a significant departure from a bi-Maxwellian behavior. Indeed, the presence of a nonthermal, high-energy tail in the electron energy distribution has been shown to make the whistler instability less unstable in the large anisotropy regime relevant for this work (Mace & Sydora 2010). Also, our mildly relativistic electrons \((k_B T_e/m_e c^2) \approx 0.28\) should somewhat increase the pressure anisotropy threshold considered in Figure 2 (Bashir et al. 2013), which is calculated for nonrelativistic electrons.

The electron pressure anisotropy is expected to give rise to viscous heating (see Equation (1)), as has been found by previous PIC simulations (see, e.g., Riquelme et al. 2016). In order to check the importance of this heating mechanism, Figure 2(d) shows the volume-averaged electron heating rate (black) for run S2: \(d \langle U_e \rangle / dt\), and compares it with the expected electron heating rate due to anisotropic viscosity (green), which is obtained from volume-averaging \(q \Delta P_e\). We see that viscous heating accounts for essentially all of the electron heating.

### 4. Nonthermal Electron Acceleration

Figure 3 shows the electron energy spectra at different times for run S2, with the time of each spectrum shown by the color bar. After the whistler modes have reached saturation \((t \cdot s \gtrsim 0.7)\), there is a rapid growth of a nonthermal tail. By the end of the simulation \((t \cdot s = 3)\), the tail can be approximated reasonably well by a power law of spectral index \(\alpha_e \approx 3.7\).7 The magenta lines show that by \(t \cdot s = 3\) the spectral index is still decreasing, although significantly slower than between \(t \cdot s \sim 1\) and \(\sim 2.5\), when it experiences its fastest evolution. The peak of the spectrum (representing its “thermal” component) also shifted to larger energies (by a factor \(\sim 1.5\)) during the simulation, which is consistent with the overall electron heating.

#### 4.1. The Acceleration Mechanism

In order to understand the origin of the nonthermal tail, we calculated the average change in the electron Lorentz factors, \(\langle \Delta \gamma \rangle\), as a function of time for two different electron groups. One group represents the electrons from the power-law tail (hereafter, the “nonthermal” electrons), which are picked so that at \(t \cdot s = 3\) they have \(\gamma > 10\). The other group belongs to the bulk of the energy distribution (the “thermal” electrons) and are chosen so that at \(t \cdot s = 3\), \(0.99 < \gamma_1 < 1\). These nonthermal and thermal electrons are marked by the gray area and by the vertical red line in Figure 3, and their \(\langle \Delta \gamma \rangle\)

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6 The whistler wave number at marginal stability satisfies \(k R_{te} = (\Delta P_e / \rho_0 e)^{1/2} (\rho_0 e)^{1/2}\) (Yoon et al. 2011), which means \(k R_{te} \sim 0.4\) for run S2 at \(t \cdot s = 2\) (see \(\Delta P_e / \rho_0 e\) from Figure 2).

7 We chose the threshold criterion \(\gamma_0 = 5\), since this is the threshold that reproduced best the \(\Delta P_e\) evolution in Riquelme et al. (2016), where \(2 \lesssim \beta \lesssim 20\), also be seen from the exponential growth of \(\langle \delta B \rangle\) in Figure 2(a) at \(t \cdot s \sim 0.7\). This growth is dominated by \(\delta B_z\), as expected for the nearly parallel whistler modes. After \(t \cdot s \sim 0.7\), the growth of \(\langle \delta B \rangle\) saturates and its amplitude is maintained at a quasi-stationary level. At \(t \cdot s \gtrsim 0.7\), \(\mu_e\) decreases at a rate close to \(s\) (see Figure 2(c)), implying that the pitch-angle scattering frequency provided by \(\langle \delta B \rangle\) is of the order of \(s\).

Although the whistler anisotropy threshold and our obtained \(\Delta P_e\) evolve similarly, there is still a factor \(\sim 2\) discrepancy. One possible reason for this is the fact that the theoretical threshold is calculated using a bi-Maxwellian electron energy distribution, while as we will see below in our simulations, there is a significant departure from a bi-Maxwellian behavior. Indeed, the presence of a nonthermal, high-energy tail in the electron energy distribution has been shown to make the whistler instability less unstable in the large anisotropy regime relevant for this work (Mace & Sydora 2010). Also, our mildly relativistic electrons \((k_B T_e/m_e c^2) \approx 0.28\) should somewhat increase the pressure anisotropy threshold considered in Figure 2 (Bashir et al. 2013), which is calculated for nonrelativistic electrons.
evolutions are shown by black lines in Figures 4(a) and (b), respectively. Besides $\langle \Delta \gamma \rangle$, Figures 4(a) and (b) also show:

1. the work performed by the electric field associated with the whistler waves, hereafter the “electric work” (EW),\(^9\) which is shown by the blue line;

2. the energy gain by anisotropic viscosity (AV), caused by the pressure anisotropy of the electrons,\(^10\) which is shown by the green line;

3. and the sum of the heating by anisotropic viscosity and the electric work (AV+EW), in red line.

Figure 4(a) shows that the work done by the whistlers' electric field on the nonthermal electrons is more than two times the viscous heating rate. This implies that these electrons are mainly energized through scattering with the whistler waves. On the other hand, Figure 4(b) shows that the energy given by this electric field to the thermal electrons is negative. This implies that the scattering process on average makes the thermal electrons lose energy to the waves. The total heating of the thermal electrons is still positive, and is mainly caused by the dominant (and positive) viscous heating. The reasonably good correspondence between $\langle \Delta \gamma \rangle$ and the sum of the energization by anisotropic viscosity and by the electric work shows that these two processes account fairly well for the total heating of electrons. Also, the fact that the works done by the electric field on the nonthermal and thermal particles are positive and negative, respectively, is consistent with this electric field not affecting the average heating of the electrons, which is dominated by viscous heating (as shown in Figure 2(d)).

\(^9\) In a shearing plasma, there is also an electric field associated to the bulk plasma motion. Since our simulations are performed in the “shearing frame,” this electric field vanishes, therefore the electric field in our runs corresponds entirely to the whistler waves.

\(^10\) For each electron, this energy gain is calculated by integrating in time the quantity $sv_jv_i\gamma/c^2$, where $v_j$ is the $j$ component of the electron velocity. In a gyrotropic plasma, it can be shown that, when averaged over the electrons, this expression reproduces the heating rate given by Equation (1).

In the case of the run S2 analyzed in this section, the nonthermal tail at $t \cdot s = 3$ contains $\sim 5\%$ of the electrons and carries $\sim 15\%$ of their energy. Notice that, for the purpose of measuring these numbers, we defined the nonthermal tail through the condition $\gamma - 1 > 2$, where the spectrum is fairly well represented by a power-law tail.

Thus, in the presented acceleration scenario, the electric field of the whistler waves effectively extracts energy from the bulk of the electron distribution and pass it to a small population of electrons, which get accelerated to nonthermal energies. However, for this mechanism to be efficient, the resonant scattering by whistler modes must occur efficiently for the thermal particles, as well as for the nonthermal electrons in the tail. The resonant condition is

$$\omega - k\|v|| = \omega_{c,e}/\gamma, \quad (2)$$

where $\omega$ is the frequency of the modes, $v|$ is the electron velocity parallel to $B$, and $\omega_{c,e}$ is the nonrelativistic electron cyclotron frequency. However, the marginally stable whistler modes satisfy $\omega/\omega_{c,e} = \Delta B_p/(\Delta B_p + P_{le})$ (Yoon et al. 2011). Thus, for $\Delta B_p/P_{le} \sim 1$ (see Figure 2(b)), the resonant condition becomes $\omega_{c,e} / k\|v|| \sim k\|v||$. Thus, in order for this condition to be satisfied by the thermal electrons, one needs for $k\|R_{le} \sim 1$. For the nonthermal electrons, a similar requirement needs to be satisfied, but with $k\|$ being a factor $\sim 2$ smaller, since the typical value of $|v||$ for these populations is a factor $\sim 2$ larger than for the thermal electrons (which are the ones that define $R_{le}$).\(^11\) This means that, for the nonthermal tail to grow, one requires a moderate widening of the whistler fluctuation power spectrum.

This is indeed what happens in simulation S2, as can be seen from Figure 5. This figure shows the power spectra of whistler fluctuations at different times ranges: right after the saturation of the instability ($t \cdot s \sim 0.8$; Figure 5(a)) and after the nonthermal tail is well developed ($t \cdot s \gtrsim 2$; Figure 5(b)). After saturation, the spectra are rather narrow and peaked, with their maxima on average at $k\|R_{le}(t) \sim 0.3$. For $t \cdot s > 2$, the

\(^11\) Indeed, thermal particles in simulation S2 have on average $|v|$ $\sim 0.5c$, while for the nonthermal ones $|v| \sim c$. 

![Figure 3](image3.png) 

**Figure 3.** Electron energy spectra at different times for S2; the time corresponding to each spectrum is shown by the color bar. After the whistler modes have reached saturation ($t \cdot s \gtrsim 1$), there is a rapid growth of a nonthermal tail. By $t \cdot s = 3$, the tail can be modeled by a power law ($dn/d\gamma \propto (\gamma - 1)^{-1}$) of spectral index $\alpha_s \sim 3.7$.

![Figure 4](image4.png) 

**Figure 4.** Panels (a) and (b) show the average change in the electron Lorentz factor $\langle \Delta \gamma \rangle$ (black line) for two groups of “nonthermal” and “thermal” electrons (marked by the gray area and vertical red line in Figure 3, respectively). In both panels, the blue line corresponds to the work done by the electric field associated with the whistler waves, or “electric work” (EW). The green line corresponds to the energy gain by anisotropic viscosity (AV). The red line corresponds to the sum of the electric work and the heating by anisotropic viscosity (EW+AV). Notice that in panel (a) the red and black lines completely overlap.
spectra widen significantly, and have on average significant power between $k_B R_{cs}$, have resonantly couple to the waves and be stochastically accelerated.

In the following sections, we analyze how the efficiency of this acceleration depends on different plasma parameters.

4.2. Dependence on $\beta_{e,\text{init}}$

Figure 6(a) shows the final spectra (at $t \cdot s = 3$) of four simulations where the electrons have the same initial temperature and magnetization ($k_B T_e = 0.28m_e c^2$ and $\omega_e/s = 1200$), but have different $\beta_{e,\text{init}}$. The four cases considered have $\beta_{e,\text{init}} = 1$ (black), 2 (red), 5 (blue), and 10 (green); the black dotted line shows the case of a Maxwell–Boltzmann distribution. We see that the hardness of the nonthermal tail gradually decreases as $\beta_{e,\text{init}}$ increases, with the $\beta_{e,\text{init}} = 1$ and 2 cases being quite similar. In Figure 6(b), we compare the spectra for $\beta_{e,\text{init}} = 2$ and 5 (solid red and solid blue lines, respectively) with power laws of spectral indices $\alpha_e = 3.7$ and 4.2 (black and green lines, respectively; $dn/d\gamma \propto (\gamma - 1)^{-\alpha_e}$). We see that these power-law indices provide a reasonably good approximation to the nonthermal tails in the $\beta_{e,\text{init}} = 2$ and 5 cases. Also, $\omega_e/s$ almost does not change the nonthermal tails, implying that the magnetization in our runs does not play a significant role in the electron acceleration.

5. Summary and Discussion

In this work, we used 2D PIC simulations to show that, in the context of a magnetic field amplified by shear plasma motion, the process of electron heating by anisotropic viscosity can give rise to a prominent electron nonthermal tail. Indeed, for $\beta_{e,\text{init}} \sim 1$ and after the field is amplified by a factor $\sim 3$, the electron energy spectrum (measured when $\beta_e \sim 0.1$, because of field amplification) contains a nonthermal power-law tail with spectral index $\sim 3.7$ (see Figure 3). The nonthermal tail contains $\sim 5\%$ of the electrons, and $\sim 15\%$ of their energy. However, the nonthermal tail becomes progressively softer as $\beta_{e,\text{init}}$ grows (see Figure 6). This behavior is in accordance with the decrease in the overall viscous heating of the electrons as $\beta_{e,\text{init}}$ increases, since this heating constitutes the ultimate source of energy for the tail formation.

The role of the whistler instability is key in the electron acceleration process. First, the whistler waves regulate the overall electron energization by determining the efficiency of the electron heating by anisotropic viscosity. This is done by providing an electron pitch-angle scattering rate comparable to the plasma shearing rate, $s$. This keeps the electron pressure anisotropy at a quasi-steady level, which is roughly determined
by the whistler instability threshold for growth rate comparable to \( s \). Second, the whistler waves drive the formation of the nonthermal tail by transferring a significant part of their energy (ultimately gained through the heating by anisotropic viscosity) to a small fraction of electrons. Thus, effectively, the whistler waves subtract energy from the bulk of the distribution and pass it to the electrons that end up forming the tail. This is inferred from the negative and positive work performed by the whistler electric field on the electrons of the thermal and nonthermal part of the energy spectrum, respectively (see Figure 4).

The present work focused on mildly relativistic electrons, with an initial temperature of \( k_B T_e = 0.28 m_e c^2 \). Previous theoretical studies have shown that stochastic electron acceleration by whistler waves should be sensitive to the ratio \( \omega_{pe}/\omega_{pe} \) (Dermer et al. 1996; Petrosian & Liu 2004). This sensitivity can be seen as a dependence on \( k_B T_e/m_e c^2 \), since for a given value, \( \beta_e, \omega_{pe}/\omega_{pe} \) uniquely fixes \( k_B T_e/m_e c^2 \). We thus defer to a future work the study of the dependence of the presented acceleration process on \( k_B T_e/m_e c^2 \). It will also be interesting to explore more extensively the regime \( \beta_e,init \ll 1 \), where the dominant whistler modes are expected to adopt a more oblique orientation, which may affect the way the proposed nonthermal acceleration works (Gary et al. 2011).

Our proposed acceleration process is likely relevant for low-luminosity accretion flows around black holes, like in Sgr A*.

For the specific case of Sgr A*, mildly relativistic electron temperatures and nonthermal spectral components with power-law indices \( \alpha \sim 3.5 \) are favored by multi-wavelength observations (Özel et al. 2000; Yuan et al. 2003; Ball et al. 2016). It is important to caution, however, that the proposed factor \( \sim 3 \) amplification of the local magnetic field may not be so common in the context of a typical turbulent accretion flow. Nevertheless, one could alternatively picture this acceleration to happen due to the cumulative effect of successive (smaller amplitude) growths and reductions of the ambient magnetic field in a turbulent medium. We will study this last possibility in a future work.

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12 Petrovian & Liu (2004) showed that the stochastic acceleration of electrons by whistler waves is more efficient for larger values of \( \omega_{pe}/\omega_{pe} \), which, for a fixed \( \beta_e \), implies larger values of \( k_B T_e/m_e c^2 \).