Time-dependent $CP$-violation parameters in $B^0 \to \eta'K^0$ decay

The BABAR Collaboration

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Abstract

We present measurements of time-dependent $CP$-violation asymmetries for the decays $B^0 \to \eta'K^0$. The data sample corresponds to 347 million $B\bar{B}$ pairs produced by $e^+e^-$ annihilation at the $\Upsilon(4S)$ resonance in the PEP-II collider, and collected with the BABAR detector. The preliminary results are $S = 0.55 \pm 0.11 \pm 0.02$, and $C = -0.15 \pm 0.07 \pm 0.03$, where the first error quoted is statistical, the second systematic.

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1 INTRODUCTION

Measurements of time-dependent CP asymmetries in $B^0$ meson decays through a dominant Cabibbo-Kobayashi-Maskawa (CKM) favored $b \rightarrow c\bar{c}s$ amplitude [1] have provided a crucial test of the mechanism of CP violation in the Standard Model (SM) [2]. For such decays the interference between this amplitude and $B^0\bar{B}^0$ mixing is dominated by the single phase $\beta = \arg \left(-V_{cd}V_{cb}^*/V_{td}V_{tb}\right)$ of the CKM mixing matrix. Decays of $B^0$ mesons to charmless hadronic final states such as $\eta'K_0$ proceed mostly via a single loop (penguin) amplitude with the same weak phase as the $b \rightarrow c\bar{c}s$ transition [3], but CKM-suppressed amplitudes and multiple particles in the loop introduce additional weak phases whose contribution may not be negligible [4, 5, 6, 7, 8].

For the decay $B^0 \rightarrow \eta'K^0$, these additional contributions are expected to be small within the SM, so the time-dependent asymmetry measurement for this decay provides an approximate measurement of $\sin^2\beta$. Theoretical bounds for the small deviation $\Delta S$ between the time-dependent CP-violation parameter $S$ measured in this decay and in the charmonium-$K^0$ decays have been calculated with an SU(3) analysis [4, 5] from measurements of $B^0$ decays to pairs of neutral light pseudoscalar mesons [9, 10]. The most stringent of these is given by Eq. 19 in [5], which assumes negligible contributions from exchange and penguin annihilation, and has a theoretical uncertainty less than $\sim 0.03$. With newer measurements [11] we obtain an improved bound $\Delta S < 0.08$ [12]. QCD factorization calculations conclude that $\Delta S$ is even smaller [7]. A significantly larger $\Delta S$ could arise from non-SM amplitudes [8].

The time-dependent CP-violation asymmetry in the decay $B^0 \rightarrow \eta'K^0$ has been measured previously by the BABAR [13] and Belle [14, 15] experiments. In this paper we update our previous measurements with an improved analysis and a data sample 1.5 times larger.

2 THE BABAR DETECTOR AND DATASET

The data were collected with the BABAR detector [16] at the PEP-II asymmetric-energy $e^+e^-$ collider [17]. An integrated luminosity of 316 fb$^{-1}$, corresponding to 347 million $B\bar{B}$ pairs, was recorded at the $\Upsilon(4S)$ resonance (center-of-mass energy $\sqrt{s} = 10.58$ GeV).

Charged particles from $e^+e^-$ interactions are detected, and their momenta measured, by a combination of five layers of double-sided silicon microstrip detectors and a 40-layer drift chamber, both operating in the 1.5 T magnetic field of a superconducting solenoid. Photons and electrons are identified with a CsI(Tl) electromagnetic calorimeter (EMC). Further charged particle identification (PID) is provided by the average energy loss ($dE/dx$) in the tracking devices and by an internally reflecting ring imaging Cherenkov detector (DIRC) covering the central region. The instrumented flux return (IFR) of the magnet allows discrimination of muons from pions.

3 ANALYSIS METHOD

3.1 Time evolution of a $B^0\bar{B}^0$ pair

From a candidate $B\bar{B}$ pair we reconstruct a $B^0$ decaying into the CP eigenstate $f = \eta'K_0^0$ or $f = \eta'K_L^0$ ($B_{CP}$). From the remaining particles in the event we also reconstruct the vertex of the other $B$ meson ($B_{tag}$) and identify its flavor. The difference $\Delta t \equiv t_{CP} - t_{tag}$ of the proper decay times $t_{CP}$ and $t_{tag}$ of the signal and tag $B$ mesons, respectively, is obtained from the measured distance between the $B_{CP}$ and $B_{tag}$ decay vertices and from the boost ($\beta\gamma = 0.56$) of the $e^+e^-$...
system. The $\Delta t$ distribution is given by:

$$F(\Delta t) = \frac{e^{-|\Delta t|/\tau}}{4\tau}[1 \pm \Delta w \pm (1 - 2w)(S\sin(\Delta m_d\Delta t) - C\cos(\Delta m_d\Delta t))].$$  \hfill (1)$$

The upper (lower) sign denotes a decay accompanied by a $B^0 (B^0)$ tag, $\tau$ is the mean $B^0$ lifetime, $\Delta m_d$ is the mixing frequency, and the mistag parameters $w$ and $\Delta w$ are the average and difference, respectively, of the probabilities that a true $B^0$ is incorrectly tagged as a $B^0$ or vice versa. The tagging algorithm [18] has six mutually exclusive tagging categories based on quantities such as the sign of charge of a lepton, kaon, or soft pion from $D^*$, grouped according to their response purities. The measured analyzing power, defined as efficiency times $(1 - 2w)^2$ summed over all categories, is (30.4±0.3)%, as determined from a large sample of $B$-decays to fully reconstructed flavor eigenstates ($B_{\text{flav}}$). The parameter $C$ measures direct CP violation. If $C = 0$, then $S = -\eta\sin 2\beta + \Delta S$, where $\eta$ is the CP eigenvalue of the final state ($-1$ for $\eta K^0_S$; $+1$ for $\eta K^*_L$).

### 3.2 Event selection

We establish the event selection criteria with the aid of a detailed Monte Carlo (MC) simulation of the $B$ production and decay sequences, and of the detector response [19]. These criteria are designed to retain signal events with high efficiency. Applied to the data, they result in a sample much larger than the expected signal, but with well characterized backgrounds. We extract the signal yields from this sample with a maximum likelihood (ML) fit.

The $B$-daughter candidates are reconstructed through their decays $\pi^0 \rightarrow \gamma\gamma$; $\eta \rightarrow \eta\gamma$ ($\eta_{\gamma\gamma}$), $\eta \rightarrow \pi^+\pi^-\pi^0$ ($\eta_{3\pi}$), $\eta' \rightarrow \eta\gamma\pi^+\pi^-$ ($\eta'_{\eta\gamma\pi^+\pi^-}$), $\eta' \rightarrow \eta_{3\pi}\pi^+\pi^-$ ($\eta'_{\eta_{3\pi}\pi^+\pi^-}$), $\eta' \rightarrow \rho^0\gamma$ ($\eta'_{\rho^0\gamma}$), where $\rho^0 \rightarrow \pi^+\pi^-$, $K^0_S \rightarrow \pi^+\pi^-$ ($K^0_{S+}$) or $\pi^0\pi^0$ ($K^0_{S0}$). Table 1 lists the requirements on the invariant mass of these particles' final states. Secondary charged pions in $\eta'$ and $\eta$ candidates are rejected if classified as protons, kaons, or electrons by their DIRC, $dE/dx$, and EMC PID signatures. We require $K^0_S$ candidates to have a flight length with significance $>3\sigma$. Signal $K^0_L$ candidates are reconstructed from clusters of energy deposited in the EMC or from hits in the IFR not associated with any charged track in the event. From the cluster centroid and the $B^0$ decay vertex we determine the direction (but not the magnitude) of the $K^0_L$ momentum $p_{K^0_L}$.

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**Table 1:** Selection requirements on the invariant masses of resonances and the laboratory energies of photons from their decay.

| State           | Invariant mass (MeV) | $E(\gamma)$ (MeV) |
|-----------------|----------------------|-------------------|
| $\pi^0$ (from $\eta_{3\pi}$) | $120 < m(\gamma\gamma) < 150$ | $> 30$ |
| $\pi^0$ (from $K^0_{S0}$) | $120 < m(\gamma\gamma) < 155$ | $> 30$ |
| $\eta_{\gamma\gamma}$ | $490 < m(\gamma\gamma) < 600$ | $> 50$ |
| $\eta_{3\pi}$ | $520 < m(\pi^+\pi^-\pi^0) < 570$ | --- |
| $\eta_{\eta\pi\pi}$ | $945 < m(\pi^+\pi^-\eta) < 970$ | --- |
| $\eta'_{\rho^0\gamma}$ | $930 < m(\pi^+\pi^-) < 980$ | $> 100$ |
| $K^0_{S+}$ | $470 < m(\pi^+\pi^-) < 980$ | --- |
| $K^0_{S0}$ | $486 < m(\pi^+\pi^-) < 510$ | --- |

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For decays with a $K_0^0$ we reconstruct the $B$-meson candidate by combining the four-momenta of the $K_0^0$ and $\eta'$ and imposing a vertex constraint. Since the natural widths of the $\eta$, $\eta'$, and $\pi^0$ are much smaller than the resolution, we also constrain their masses to world-average values [20] in the fit of the $B$ candidate. From the kinematics of $\Upsilon(4S)$ decay we determine the energy-substituted mass $m_{ES} \equiv \sqrt{(\frac{1}{2} s + p_0 \cdot p_B)^2 / E_{0}^2 - p_B^2}$ and the energy difference $\Delta E \equiv E_B^* - \frac{1}{2} \sqrt{s}$. where $(E_0, p_0)$ and $(E_B, p_B)$ are four-momenta of the $\Upsilon(4S)$ and the $B$ candidate, respectively, and the asterisk denotes the $\Upsilon(4S)$ rest frame. The resolution in $m_{ES}$ is 3.0 MeV and in $\Delta E$ is 20 – 50 MeV, depending on the decay mode. We require $5.25 < m_{ES} < 5.29$ GeV and $|\Delta E| < 0.2$ GeV ($-0.01 < \Delta E < 0.08$ GeV for $B^0 \to \eta'K_0^0$).

For a $B^0 \to \eta'K^0_L$ candidate we obtain $\Delta E$ and $p_{K^0_L}$ from a fit with $B^0$ and $K^0_L$ masses constrained to their accepted values [20]. To make a match with the measured $K^0_L$ direction we construct the missing momentum $p_{\text{miss}}$ from $p_0$ and all charged tracks and neutral clusters other than the $K^0_L$. We then project $p_{\text{miss}}$ onto $p_{K^0_L}$, and require the component perpendicular to the beam line, $p_{\text{proj}}$, to satisfy $p_{\text{proj}}^2 > -0.5$ GeV/c. This value reflects the resolution, and was chosen to minimize the yield uncertainty in the presence of continuum background.

For all $B^0 \to \eta'K^0$ candidates we require for $\Delta t$ and its error $\sigma_{\Delta t}$, $|\Delta t| < 20$ ps and $\sigma_{\Delta t} < 2.5$ ps.

### 3.3 Background rejection

Backgrounds arise primarily from random combinations of particles in continuum $e^+e^- \to q\bar{q}$ events ($q = u, d, s, c$). We reduce these with requirements on the angle $\theta_T$ between the thrust axis of the $B$ candidate in the $\Upsilon(4S)$ frame and that of the rest of the charged tracks and neutral calorimeter clusters in the event. The distribution is sharply peaked near $|\cos \theta_T| = 1$ for $q\bar{q}$ jet pairs, and nearly uniform for $B$-meson decays. The requirement, which optimizes the expected signal yield relative to its background-dominated statistical error, is $|\cos \theta_T| < 0.9$ ($|\cos \theta_T| < 0.8$ for $B^0 \to \eta'K^0_L$).

In the ML fit we discriminate further against $q\bar{q}$ background with a Fisher discriminant $F$ that combines several variables which characterize the production dynamics and energy flow in the event [10]. It provides about one standard deviation of separation between $B$ decay events and combinatorial background.

For the $\eta'\rho$ decays we require $|\cos \theta_{\text{dec}}| < 0.9$ to exclude the most asymmetric decays where soft-particle backgrounds concentrate and the acceptance changes rapidly. Here $\theta_{\text{dec}}$ is the angle between the momenta of the $\rho^0$ daughter $\pi^-$ and the $\eta'$, measured in the $\rho^0$ rest frame.

For $B^0 \to \eta'K^0_L$ candidates we require that the cosine of the polar angle of the total missing momentum in the laboratory system be less than 0.95, to reject very forward $q\bar{q}$ jets. The purity of the $K^0_L$ candidates reconstructed in the EMC is further improved by a requirement on the output of a neural network (NN) that takes cluster-shape variables as its inputs. The NN was trained on MC signal events and data events in the sideband $0.04 < \Delta E < 0.08$ GeV. We checked the performance of the NN with $K^0_L$ candidates in the larger $B^0 \to J/\psi K^0_L$ sample.

The average number of candidates found per selected event is in the range 1.08 to 1.32, depending on the final state. We choose the candidate with the smallest value of a $\chi^2$ constructed from the deviations from expected values of one or more of the daughter resonance masses, or with the best vertex probability for the $B$, depending on the decay channel. In $B^0 \to \eta'K^0_L$ if several $B$ candidates have the same vertex probability, we chose the candidate with the $K^0_L$ reconstructed from, in order, EMC and IFR, EMC only, or IFR only. From the simulation we find that this algorithm selects the correct-combination candidate in about two thirds of the events containing
multiple candidates, and that it induces negligible bias.

### 3.4 Maximum likelihood fit

We obtain the common $CP$-violation parameters and yields for each channel from a maximum likelihood fit with the input observables $\Delta E$, $m_{ES}$, $F$, and $\Delta t$. The selected sample sizes are given in the first column of Table 2. Besides the signal events they contain $q\bar{q}$ (dominant) and $b\bar{b}$ with $b \to c$ combinatorial background, and a fraction that we estimate from the simulation to be less than 1.1% of cross feed from other charmless $B\bar{B}$ modes. The charmless events (henceforth referred to as $B\bar{B}$) have ultimate final states different from the signal, but similar kinematics, and exhibit broad peaks in the signal regions of some observables. We account for these with a separate component in the probability density function (PDF). For each component $j$ (signal, $q\bar{q}$ combinatorial background, or $B\bar{B}$ background) and tagging category $c$, we define a total probability density function for event $i$ as

$$P_{j,c}^i \equiv P_j(m_{ES}^i) \cdot P_j(\Delta E^i) \cdot P_j(F^i) \cdot P_j(\Delta t^i, \sigma_{\Delta t}; c),$$

except for $B^0 \to \eta'K_L^0$ for which $P_j(m_{ES}^i)$ is omitted. The factored form of the PDF is a good approximation, particularly for the combinatorial $q\bar{q}$ component, since correlations among observables measured in the data (in which $q\bar{q}$ dominates) are small. Distortions of the fit results caused by this approximation are measured in simulation and included in the bias corrections and systematic errors discussed below.

With $Y_j$ defined to be the yield of events of component $j$, and $f_{j,c}$ the fraction of events of component $j$ for each category $c$, we write the extended likelihood function for all events belonging to category $c$ as

$$L_c = \exp \left( - \sum_j Y_j f_{j,c} \prod_i (Y_{\text{sig}} f_{\text{sig},c} P_{\text{sig},c}^i + Y_{q\bar{q}} f_{q\bar{q},c} P_{q\bar{q}}^i + Y_{BB} f_{BB,c} P_{BB}^i) \right),$$

where $N_c$ is the number of events of category $c$ in the sample. We found that the $B\bar{B}$ background component is needed only for the channels with $\eta'^{u,v}$. We fix both $f_{\text{sig},c}$ and $f_{BB,c}$ to the values measured with the large $B_{\text{flav}}$ sample [21]. The total likelihood function $L_d$ for decay mode $d$ is given as the product over the six tagging categories. Finally, when combining decay modes we form the grand likelihood $L = \prod L_d$.

The PDF $P_{\text{sig}}(\Delta t, \sigma_{\Delta t}, c)$ is given by $F(\Delta t)$ (Eq. 1) with tag category ($c$) dependent mistag parameters convolved with the signal resolution function (a sum of three Gaussians) determined from the $B_{\text{flav}}$ sample. We determine the remaining PDFs for the signal and $B\bar{B}$ background components from fits to MC data, for which the resolutions in $\Delta E$ and $m_{ES}$ are calibrated with large control samples of $B$ decays to charmed final states of similar topology (e.g. $B \to D(K\pi\pi\pi)$). For the combinatorial background the PDFs are determined in the fits to the data. However we first deduce the functional form from a fit of each component alone to a sideband in $(m_{ES}, \Delta E)$, so that we can validate the fit before applying it to data containing the signal.

These PDF forms are: the sum of two Gaussians for $P_{\text{sig}}(m_{ES})$ and $P_{\text{sig}}(\Delta E)$; the sum of three Gaussians for $P_{q\bar{q}}(\Delta t; c)$; a conjunction of two Gaussian segments below and above the peak with different widths for $P_j(F)$ (a small “tail” Gaussian is added for $P_{\text{sig}}(F)$); a linear dependence for $P_{q\bar{q}}(\Delta E)$; and for $P_{q\bar{q}}(m_{ES})$ the function $x\sqrt{1-x^2}\exp[-\xi(1-x^2)]$, with $x = 2m_{ES}/\sqrt{s}$. These are discussed in more detail in [10].

We allow the parameters most important for the determination of the combinatorial background PDFs to vary in the fit. Thus for the six channels listed in Table 2 we perform a single fit with
We test and calibrate the fitting procedure by applying it to ensembles of simulated q̅q̅ experiments drawn from the PDF into which we have embedded the expected number of signal and B̅B̅ background events randomly extracted from the fully simulated MC samples. We find negligible bias for C. For S we find and apply multiplicative correction factors for bias from dilution due to B̅B̅ background, equal to 1.02 in the final states η′K^0 and ηK^0, and 1.05 in η′K^0_ππ̅.

### 3.5 Fit Results

| Mode                      | Events to fit | Signal yield | −ηS   | C         |
|---------------------------|---------------|--------------|-------|-----------|
| η′(γγ)K^0_π+π−            | 612           | 206 ± 16     | 0.60 ± 0.24 | −0.26 ± 0.14 |
| η′K^0_π+π−                | 10905         | 503 ± 28     | 0.50 ± 0.15 | −0.26 ± 0.11 |
| η′(3π)πK^0_π+π−           | 164           | 63 ± 8       | 0.85 ± 0.38 | 0.24 ± 0.26 |
| η′η′(γγ)K^0_π0π0          | 446           | 50 ± 9       | 0.77 ± 0.44 | −0.25 ± 0.36 |
| η′η′K^0_π0π0              | 12559         | 114 ± 23     | 0.42 ± 0.47 | 0.30 ± 0.30 |
| η′K^0_0                   | 3389          | 168 ± 21     | 0.39 ± 0.30 | 0.20 ± 0.23 |
| η′K^0                    | 0.55 ± 0.11   | −0.15 ± 0.07 |

Figure 1: Distributions projected onto (a) m_ES and (b) ΔE for B^0 → η′K^0 candidates.

Results from the fit for the signal yields and the CP parameters S and C are presented in Table 2. In Fig. 1 we show for B^0 → η′K^0 the projections onto m_ES and ΔE for a subset of the data for which the signal likelihood (computed without the variable plotted) exceeds a mode-dependent threshold that optimizes the sensitivity; the corresponding distribution in ΔE for B^0 → η′K^0 is
Figure 2: Distribution projected onto $\Delta E$ for $B^0 \rightarrow \eta' K^0_L$ candidates. Points with error bars represent the data, the solid line the fit function, and the dashed line its background component.

Given in Fig. 2, Fig. 3 gives the $\Delta t$ projections and asymmetry of the combined modes for events selected as for Figs. 1 and 2. We measure a correlation of 3.0% between $S$ and $C$ in the fit.

We perform numerous crosschecks of our fitter: time-dependent fits for $B^+$ decays to the charged final states $\eta'_{\gamma(\gamma\gamma)}\pi\pi K^+$, $\eta'_{\gamma\gamma} K^+$, and $\eta'_{\eta(3\pi)}\pi\pi K^+$; fits removing one fit variable at a time; fits without $B\overline{B}$ PDFs; fits with multiple $B\overline{B}$ components; fits allowing for non-zero CP information in $B\overline{B}$ events; fits with $C = 0$ and others. In all cases, we find results consistent with expectation. The value $S_{\eta'K^0_S} = 0.57 \pm 0.11$ is larger than our previous measurement $S_{\eta'K^0_S} = 0.30 \pm 0.14$ [13] as a result of the larger data sample and events added or removed as a result of changes in the reconstruction and selection. For events common to the two datasets we find close agreement of the values of $S$ and $C$.

Figure 3: Projections onto $\Delta t$ for (a-c) $B^0 \rightarrow \eta' K^0_S$ and (d-f) $B^0 \rightarrow \eta' K^0_L$ of the data (points with error bars), fit function (solid line), and background function (dashed line), for (a, d) $B^0$ and (b, e) $B^0$ tagged events, and (c, f) the asymmetry between $B^0$ and $B^0$ tags.
3.6 Systematic studies

We find systematic uncertainties from several sources (in decreasing order of magnitude): variation of the signal PDF shape parameters within their errors, modeling of the signal $\Delta t$ distribution, use of $\Delta t$ signal parameters from the $B_{\text{flav}}$ sample, interference between the CKM-suppressed $\bar{b} \to \bar{u} c d$ amplitude and the favored $b \to c u d$ amplitude for some tag-side $B$ decays [22], $B \bar{B}$ background, SVT alignment, and position and size of the beam spot. The $B_{\text{flav}}$ sample is used to determine the errors associated with the signal $\Delta t$ resolutions, tagging efficiencies, and mistag rates. We take the uncertainties in $\tau_B$ and $\Delta m_d$ from the published measurements [20]. Summing all systematic errors in quadrature, we obtain 0.02 for $S$ and 0.03 for $C$.

4 RESULTS AND DISCUSSION

In conclusion, we have used samples of about 940 $B^0 \to \eta' K^0_S$ and 170 $B^0 \to \eta' K^0_L$ events to measure the time-dependent $CP$ violation parameters in $B^0 \to \eta' K^0$ $S = 0.55 \pm 0.11 \pm 0.02$ and $C = -0.15 \pm 0.07 \pm 0.03$. Our result for $S$ is consistent with the world average of those measured in $B^0 \to J/\psi K^0_S$ [18, 15], and inconsistent with zero ($CP$ conservation) by 4.9 standard deviations. Our result for the direct-$CP$ parameter $C$ is 1.8 standard deviations from zero. The results are preliminary.

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