Ultracold Rb-OH collisions and prospects for sympathetic cooling

Manuel Lara,1 John L. Bohn,1 Daniel Potter,2 Pavel Soldán,3 and Jeremy Hutson2
1JILA, NIST and Department of Physics, University of Colorado, Boulder, CO 80309-0440
2Department of Chemistry, University of Durham, South Road, Durham, DH1 3LE, United Kingdom
3Doppler Institute, Department of Physics, Faculty of Nuclear Sciences and Physical Engineering, Czech Technical University, Břehová 7, 115 19 Praha 1, Czech Republic

(Dated: September 11, 2018)

We have computed ab initio cross sections for cold collisions of Rb atoms with OH radicals. We predict collision rate constants of order $10^{-11}$ cm$^3$/s at temperatures in the range 10-100 mK at which molecules have already been produced. However, we also find that in these collisions the molecules have a strong propensity for changing their internal state, which could make sympathetic cooling of OH in a Rb buffer gas problematic in magnetostatic or electrostatic traps.

PACS numbers: 34.20.Mq, 34.50.-s, 33.80.Ps

A great way to make something cold is to place it in thermal contact with something else even colder. Thus, for many years, it has been possible to cool one species of ion sympathetically, by placing it in contact with another species that is being actively cooled [1, 2]. More recently, ultracold neutral atoms have also been sympathetically cooled [3]. At slightly higher temperatures, other species that is being actively cooled [1, 2]. More recently, ultracold neutral atoms have also been sympathetically cooled [3]. At slightly higher temperatures, atoms and molecules have been sympathetically cooled in a helium buffer gas [4]. Molecules are widely regarded as atoms and molecules have been sympathetically cooled in thermally cooled [3]. At slightly higher temperatures, molecules have already been produced. However, we also find that in these collisions the molecules have a strong propensity for changing their internal state, which could make sympathetic cooling of OH in a Rb buffer gas problematic in magnetostatic or electrostatic traps.

We begin by describing the potential energy surfaces (PES’s), and incorporating the hyperfine structure of the collision partners.

Our prototype system for this study consists of OH molecules in a bath of Rb atoms. This is a particularly timely example: the OH radical has been successfully slowed by Stark deceleration techniques in at least two laboratories, which can now produce ~ 10 mK packets of these molecules on demand [6, 8]. At the same time, Rb is easily cooled and trapped in copious quantities at tens or hundreds of µK, making it an ideal target for the molecules. In addition, the Rb-OH collision system is subject to a “harpooning” process, similar to that in Rb-NH [9], where during a collision the valence electron jumps from Rb to OH [10]. This process is without precedent in the cold collisions literature. Thus, even apart from sympathetic cooling, the Rb-OH scattering system is quite rich from a cold collisions perspective.

We begin by describing the potential energy surfaces (PES’s) of the system, as functions of $(R, \theta)$, where $R$ is the distance between the atom and diatom, and $\theta$ is the angle that the Jacobi vector $\vec{R}$ makes with the OH axis. The OH monomer has a $^2\Pi$ ground state arising from a $\pi^2$ configuration, while the ground state of Rb is $^2S$. This produces $^1\Pi$ and $^3\Pi$ states for linear ROH, which split into $^1A'$, $^1A''$ and $^3A'$, $^3A''$ surfaces at nonlinear geometries. We will refer to these as the covalent states. In addition, RbOH has an ion-pair state analogous to the ones previously found for RbNH [8]. The ion-pair threshold for Rb$^+$ ($^1S$) + OH$^-$ ($^1\Sigma^+$) lies only 2.35 eV above the ground state at $R = \infty$ and produces a $^1\Sigma^+$ ($^1A'$) state that cuts steeply down, crossing the covalent states near 6 Å. This is an actual crossing at linear geometries, where the ion-pair and covalent states have different symmetries, but there are avoided crossings between the two
states of $^{1}A'$ symmetry at nonlinear geometries. There is therefore a conical intersection between the two $^{1}A'$ surfaces at linear geometries.

Potential energy surfaces for all 5 electronic states of RbOH were calculated by complete active space self-consistent field (CASSCF) calculations followed by multireference configuration interaction (MRCI). A full description will be given elsewhere. All calculations used the MOLPRO package with aug-cc-pVTZ basis sets in uncontracted form for O and H and the ECP28MWB small-core quasirelativistic effective core potential for Rb, with the valence basis set from Ref. 13. The CASSCF calculation included all configurations that can be formed from the lowest (10,3) orbitals of $(a', a'')$ symmetry, with the lowest (5,1) orbitals doubly occupied. Energies were calculated in Jacobi coordinates $(R, \theta)$ on a grid of 25 unequally spaced points in $R$ from 2 to 12 Å and 11 Gauss-Lobatto quadrature points in $\theta$. The two $^{1}A'$ surfaces were transformed to obtain two quasidiabatic diagonal surfaces and a coupling surface, using a mixing angle derived from matrix elements of the OH $\hat{L}_z$ operator. Finally, the quasidiabatic covalent energies were extrapolated to $R = \infty$ using $C_6$ and $C_7$ coefficients obtained from coupled cluster (CCSD) calculations at $R = 15, 25$ and 100 Å. The singlet and triplet sum and difference surfaces were expanded in normalized associated Legendre functions and the radial coefficients were interpolated using the reciprocal-power reproducing kernel Hilbert space (RP-RKHS) method.

The resulting diabatic covalent surfaces have wells 337 and 511 cm$^{-1}$ deep at linear Rb-OH geometries for the singlet and triplet surfaces respectively. For the $A'$ surfaces this linear well is the absolute minimum, but the $A''$ surfaces have absolute minima at non-linear geometries ($\theta \approx 125^\circ$) with depths of 405 and 615 cm$^{-1}$ respectively. The ion-pair state is very much deeper, with a well $\approx 26000$ cm$^{-1}$ below the neutral threshold.

To perform scattering calculations on these surfaces, we expand the wave function into an appropriate basis set. This set will consist of the quantum numbers of the atom and diatom in the separated limit. For the atom, electronic ($s_a$) and nuclear ($i_a$) spins are coupled to make total spin $|f_a m_{f_a}\rangle$ in the lab frame. For the diatom, the electronic wave function is specified in Hund’s coupling case (a) by the total electronic angular momentum $j$, with projections $m$ in the lab frame and $\omega$ in the frame rotating with the molecule. As usual, $\omega$ is separated into its orbital and spin components, $\omega = \lambda + \sigma$. Linear combinations $|\lambda\omega\rangle = (|\lambda\omega\rangle + |\lambda - \omega\rangle)/\sqrt{2}$ are constructed to produce states of good parity appropriate to the zero-electric-field case we consider here. Finally, $j$ is coupled to the nuclear spin $i_a$ of the hydrogen atom to yield total diatom spin $|f_a m_{f_a}\rangle$. The partial wave quantum numbers $|LM_L\rangle$ account for the relative orientation of the collision pair in the lab frame. Thus the basis states of our calculation are given by

$$|s_d\lambda\omega\epsilon(f_d m_{f_d})|(s_a i_a)f_a m_{f_a}|LM_L\rangle.$$ (1)

In this basis the total parity $p = \epsilon(-1)^{j - s_d + L}$ and the lab-projection of total angular momentum, $m_d + m_a + M_L$, are conserved quantities. In zero field, the total angular momentum $\mathcal{F} = f_d + f_a + L$ would also be conserved; however, we anticipate considering the action of a field on the collisions, which would mix different $\mathcal{F}$ values. We therefore do not exploit this symmetry here.

Cast in this basis, the Schrödinger equation for Rb-OH collisions takes the standard form of a set of close-coupled equations in the variable $R$. To solve these, we propagate the log-derivative matrix $Y$ $\equiv \psi^{-1}d\psi/dR$ using a variable-step version of Johnson’s algorithm. Because of the multiple PES’s and the inclusion of hyperfine degrees of freedom, the total number of scattering channels required to solve the complete problem including spin (in excess of 25,000) is prohibitively large.

To overcome this obstacle, we exploit a kind of frame-transformation procedure. We identify a suitable radius $R = R_0$, and define $R < R_0$ and $R > R_0$ as the “short-range” and “long-range” parts of the calculation, respectively. For Rb-OH, we choose $R_0 = 17$ a.u. In the short-range region, the PES’s are deep, and the hyperfine effects are small. We therefore compute $Y$ in a basis of decoupled nuclear spins and neglect couplings between blocks of the Hamiltonian with different nuclear spin projections $m_{ia}$ or $m_{id}$. In this pilot study, we have neglected the influence of the ion-pair channel.

At long range, $R > R_0$, the full hyperfine structure is restored, and $Y$ is transformed into the basis (1) for further propagation and matching to spherical Bessel functions to yield scattering matrices. In this region, collision channels in which the molecule is excited into higher-lying rotational or spin-orbit states are already strongly closed. We therefore eliminate these channels. In the inner region, we use partial waves up to $L = 28$ and rotational states up to $j = 11/2$. In the outer region, we employ partial waves up to $L = 22$, but with full hyperfine structure of the $j = 3/2$ rotational ground state. Because of these approximations, no single calculation requires more than 2000 channels. Numerical checks suggest that the magnitudes of cross sections computed in this way are accurate to within a factor of $\sim 2$.

For concreteness, we calculate cross sections for a beam experiment in which the incident wave vector is coincident with the laboratory quantization axis. Energy-dependent cross sections for two different initial states of the collision partners are shown in Fig. 11. In the first case, Fig. 11(a), the Rb atom is initially in its “stretched” state, with $|f_a m_{f_a}\rangle = |22\rangle$, and the molecule is in its higher-lying, $f$ parity state, and also spin stretched, with $|f_a m_{f_a}\rangle = |22\rangle$. Both these states are weak-magnetic-field seeking, meaning that they can be trapped magnetically. In addition, OH in this state can be trapped electrically.
trostatically. Solid lines denote elastic cross sections $\sigma_{el}$, in which all internal quantum numbers are retained after the collision, and dashed lines refer to inelastic cross sections $\sigma_{inel}$, which represents the sum of partial cross sections to many possible outcomes distinct from the initial channel (including $m_a$ and $m_j$-changing collisions that do not release energy at zero field).

For collisions between S-state atoms, being in a stretched state greatly reduces inelastic cross sections. This is simply because the $m_{f_a}$ projection of one atom cannot be reduced at the expense of raising $m_{f_a}$ of the other atom. Rather, to conserve angular momentum, such a collision can occur only if the partial wave projection $M$ can change, which requires an anisotropic interaction. For two S-state atoms, the only anisotropic interaction is the magnetic dipole interaction between valence electrons, which is very weak. For Rb-OH collisions, by contrast, the PES itself is highly anisotropic, providing a ready avenue for spin-changing collisions. Indeed, inelastic scattering is as likely as, or more likely than, elastic scattering over much of the energy range. This trend is especially pronounced at low energies (below $\sim 1$ mK), where the Wigner threshold law sets in. The elastic cross section must tend to a constant at threshold, but exoergic inelastic processes must yield cross sections that diverge as $1/\sqrt{E}$. Note that the actual magnitudes of cross sections in this limit are strongly subject to details of the PES, details which are typically uncovered only by experiments. Thus the cross sections in Fig. 1 while suggestive, cannot be taken as definitive predictions.

At higher energies, many partial waves can contribute to the scattering, and the threshold laws are less significant. Because the electron spin of the OH is strongly tied to the rotating molecule, spin orientation in the lab frame is completely disrupted during a collision. This process can be approximated simply by a Langevin model [10]: for a given energy $E$, there is a maximum partial wave $L(E)$ for which $E$ lies above the centrifugal barrier of the long-range potential $-C_6/R^6 + \hbar^2 L(L+1)/2\mu R^2$. Here $C_6 = 325E_0a_0^6$ is the isotropic Van der Waals coefficient of the PES $V$, and $\mu$ the reduced mass of the collision pair. In the Langevin model, we assume that any partial wave smaller than $L(E)$ contributes to inelastic scattering with unit probability, i.e., any time the atom and molecule are near one another, they are essentially guaranteed to disrupt the electron’s spin. This idea leads to a cross section

$$\sigma_{\text{Langevin}}(E) = 3\pi \left( \frac{C_6}{4E} \right)^{1/3}.$$  

(2)

This cross section is also shown in Fig. 1(a), by the solid symbols. It is clearly getting the trend and the order of magnitude of the cross sections correct.

We therefore predict that Rb-OH elastic cross sections, at temperatures of tens of mK typical of Stark decelerators, will be on the order of $10^{-13}$ cm$^2$. At the corresponding collision velocities of several hundred cm/s, this corresponds to elastic collision rate constants on the order of $10^{-11}$ cm$^3$/s, which is easily large enough to provide sufficient thermal contact to allow sympathetic cooling in overlapped traps of OH and Rb. However, inelastic rate constants are of the same order of magnitude, which bodes ill for sympathetic cooling, at least in magnetostatic or electrostatic traps. Including the ion-pair channels would likely only disrupt the internal states more severely, and would not change this basic conclusion about sympathetic cooling.

FIG. 1: Rb-OH collision cross sections versus energy. Solid (dashed) lines represent elastic (inelastic) cross sections. In (a) is shown results for the incident channel $|^2\Pi_{3/2}, f_m J_a = 22, f\rangle_{\text{OH}} | f_m J_a = 22\rangle_{\text{Rb}}$, where both the atom and diatom are weak-magnetic-field seeking, and the OH is also weak-electric-field seeking. In (b) is shown the incident channel $|^2\Pi_{3/2}, f_m J_a = 11, e\rangle_{\text{OH}} | f_m J_a = 1 - 1\rangle_{\text{Rb}}$. Again, both species are in weak-magnetic-field seeking states, but the OH is now in a strong-electric-field seeking state. The points indicate the Langevin cross section, Eqn. (2).
We turn now to an alternative pair of initial states, whose scattering cross sections are shown in Fig. (b). Here the atom is in its lowest magnetically trappable state, with \(|f_a m_{f_a}⟩ = |1⟩ - 1⟩\), and the molecule is in its lower-energy \(e\) state, with total spin \(|f_d m_{f_d}⟩ = |11⟩\) (also magnetically trappable). At zero field, both \(σ_{el}\) and \(σ_{inel}\) are energy-independent at low energies, since all exit channels are iso-energetic with the incident channel. In nonzero field, the \(|11⟩_{OH}|1\rangle_{Rb}\) channel lies above other \(m\)-components in energy, and \(σ_{inel}\) would again diverge.

By the same token, sympathetic cooling is possible at low energies for OH molecules in the \(|1⟩ - 1⟩\) state and Rb atoms in the \(|11⟩\) state. This is the lowest-energy channel of all: there are no inelastic channels energetically available and \(σ_{inel}\) will vanish. These states are not magnetically trappable, but could be confined in an optical or microwave \([20]\) dipole trap or an alternating current trap \([21]\). A small static magnetic field will be needed to maintain the projection quantum numbers.

At higher collision energies, other forms of inelastic scattering become energetically allowed. Once the collision energy surpasses the height of the \(p\)-wave centrifugal barrier (at about 1.6 mK), the molecule can shed angular momentum into the partial wave degree of freedom. At this point \(σ_{inel}\) climbs to a large value, comparable to \(σ_{el}\). Further, at about 4mK, the \(f = 2\) hyperfine state of OH becomes energetically allowed, providing another route to inelastic collisions. By examining the partial cross sections, we find that these two avenues for inelastic collisions are roughly equally likely. At still higher collision energies, \(σ_{inel}\) is again roughly approximated by the Langevin result \([22]\), although there is now more structure, owing to a large number of Feshbach resonances to fine-and hyperfine excited states.

These results present a cautionary tale for sympathetic cooling using alkali atoms. One may regard inelastic scattering as a “Murphy’s Law” process \([22]\). Namely, if the internal state of the molecule can change to produce an unfavorable result, it will do so. The key to making sympathetic cooling viable lies in eliminating undesirable channels as far as possible. For example, a light collision partner with a small \(C_6\) coefficient will produce a centrifugal barrier at higher energy, preventing partial waves from accepting angular momentum. This circumstance explains, at least partly, the ability of a He buffer gas to cool molecules without badly disrupting spin orientation \([23], 24, 25]\). In the present context of alkali atoms, consider Li, which is about 12 times lighter than Rb, and about half as polarizable. Its \(p\)-wave centrifugal barrier upon colliding with OH is on the order of 10 mK. In addition, a molecule that is better described by Hund’s coupling case (b), in which the electron’s spin is only weakly coupled to the molecular rotation axis, may help weaken \(σ_{inel}\) below the Langevin limit \([25]\).

In summary, we have performed the first \(ab\ initiō\) scattering calculations for an open-shell, ground state molecule colliding with an alkali atom, incorporating the hyperfine structure of both collision partners. The results suggest that elastic cross sections are sufficiently large for sympathetic cooling to occur, yet equally large inelastic cross sections probably hinder this application. Nonetheless, the results do not preclude the possibility that, by applying electric or magnetic fields, inelastic cross sections could be suppressed \([21, 27]\). This will be the subject of a future study.

ML and JLB gratefully acknowledge the NSF and the W. M. Keck Foundation, PS acknowledges the MÚST CR (grant No. LC06002).

[1] R. E. Drullinger et al., Appl. Phys. 22, 365 (1980).
[2] D. J. Larson et al., Phys. Rev. Lett. 57, 70 (1986).
[3] This was first reported by C. J. Myatt et al., Phys. Rev. Lett. 78, 586 (1997).
[4] R. deCarvalho et al., Euro. Phys. J. D 7, 289 (1999).
[5] See the special issue of Euro. Phys. J. D, 31, pp. 149-145 (2004), and references therein.
[6] S. Y. T. van de Meerakker, N. Vanhaecke, and G. Meijer, Ann. Rev. Phys. Chem. 57, 159 (2005).
[7] K. M. Jones, E. Tiesinga, P. D. Lett, and P. S. Julienne, Rev. Mod. Phys. 78, 483 (2006).
[8] J. R. Bochinski, E. R. Hudson, H. J. Lewandowski, and J. Ye, Phys. Rev. A 70, 043410 (2004).
[9] P. Soldán and J. M. Hutson, Phys. Rev. Lett. 92, 163202 (2004).
[10] R. D. Levine and R. B. Bernstein, Molecular Reaction Dynamics and Chemical Reactivity (Oxford, New York, 1987).
[11] M. Lara et al., unpublished.
[12] H.-J. Werner, P. J. Knowles, R. Lindh, M. Schütz, et al., MOLPRO quantum chemistry package, version 2002.6 (2002); http://www.molpro.net/.
[13] T. H. Dunning, Jr., J. Chem. Phys. 90, 1007 (1989).
[14] T. Leininger et al., Chem. Phys. Lett. 255, 274 (1996).
[15] P. Soldán, M. T. Cvitaš, and J. M. Hutson, Phys. Rev. A 67, 054702 (2003).
[16] T. S. Ho and H. Rabitz, J. Chem. Phys. 104, 2584 (1996).
[17] P. Soldán and J. M. Hutson, J. Chem. Phys. 112, 4415 (2000).
[18] B. R. Johnson, J. Comput. Phys. 13, 445 (1973).
[19] U. Fano and A. R. P. Rau, Atomic Collisions and Spectra (Academic Press, Orlando, 1986).
[20] D. DeMille, D. R. Glenn, and J. Petricka, Euro. Phys. J. D 31, 375 (2004).
[21] J. van Veldhoven, H. L. Bethlehem, and G. Meijer, Phys. Rev. Lett. 94, 083001 (2005).
[22] R. A. J. Matthews, Proc. Roy. Inst. Gr. Br. 70, 75 (1997).
[23] J. D. Weinstein et al., Nature 395, 148 (1998).
[24] J. L. Bohn, Phys. Rev. A 61, 040702 (2000); ibid, 62, 032701 (2000).
[25] R. V. Krems, A. Dalgaro, N. Balakrishnan, and G. C. Groenenboom, Phys. Rev. A 67, 060703 (2003).
[26] C. Ticknor and J. L. Bohn, Phys. Rev. A 71, 022709 (2005).
[27] R. V. Krems, Int. Rev. Phys. Chem. 24, 99 (2005).