Enhanced Sensitivity of FeGa Thin-Film Coated SAW Current Sensor

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Abstract: A surface acoustic wave (SAW) device is proposed for sensing current by employing the patterned FeGa thin film as the sensitive interface. The layered media structure of FeGa/SiO$_2$/LiNbO$_3$ was established to reveal the working principle of the sensors, and an SAW chip patterned by delay-line and operating at 150 MHz was fabricated photolithographically on 128° YX LiNbO$_3$ substrate. The FeGa thin film with a larger magnetostrictive coefficient was sputtered onto the acoustic propagation path of the SAW chip to build the sensing device. The prepared device was connected into the differential oscillation loop to construct the current sensor. The FeGa thin film produces magnetostrictive strain and so-called $\Delta E$ effect at the magnetic field generated by the applied current, which modulates the SAW propagation velocity accordingly. The differential frequency signal was collected to characterize the measurand. Larger sensitivity of 37.9 kHz/A, low hysteresis error of 0.81%, excellent repeatability and stability were achieved in the experiments from the developed sensing device.

Keywords: surface acoustic wave; current sensor; FeGa thin film; magnetostrictive strain; $\Delta E$ effect

1. Introduction

Current sensors are widely used in current monitoring applications in smart grid line testing, metallurgical and power supplies, rail transit safety warnings and rescue, and power relay protection in industrial automation [1]. Among the available sensing technologies, the surface acoustic wave (SAW) current sensor features fast response, simple structure, low cost, excellent resistance to interference, low power consumption, and long service life [2–4]. Especially, it can realize wireless and passive measurement means to improve system security [5–7]. The specialized current sensing prototype employing the magnetoresistance effect was proposed firstly by Reindl et al. The obtained current resolution was approximately 5% of full scale (~800 A~800 A) [6]. Another typical SAW current sensing device is built by depositing magnetostrictive thin film along the acoustic propagation path of the SAW chip. The magnetostrictive thin film produces magnetostrictive strain and so-called $\Delta E$ effect at the magnetic field generated by the applied current, which modulates the SAW propagation velocity accordingly. Then the corresponding shifts in oscillation frequency are collected to evaluate the applied current information [1,8,9].

Since the pioneering work was conducted by Ganguly et al. in 1975 [10], the SAW devices for sensing current/magnetic field have attracted more interests because of their unique advantages, and meaningful results were reported from some prototypes. Using the FeCo thin film as the sensitive interface, the SAW current sensor prototype was constructed successfully, a larger sensitivity of 16.6 kHz/A was achieved, and the patterned design was considered to improve the hysteresis error [1,8,9]. A similar structure was also proposed by Tong et al.; the current sensitivity of 10.7 kHz/A was achieved by using the FeNi as the...
sensing interface [11]. Kadota et al. developed a SAW sensing chip constructed using a magnetostrictive Ni electrode on ST-cut 90°X quartz substrate [12]. Zhou et al. obtained a maximum SAW velocity shift close to 20% from a multilayered sensing structure of TbCo\textsubscript{2}/FeCo for the shear horizontal wave as a ratio close to 1 between magneto-elastic film thickness and wavelength [13]. Fahim et al. proposed a SAW magnetic sensor using Polyvinyl Alcohol (PVA) bound magnetostrictive nanopowder thin film, and a sensor response of up to 678.05 kHz was obtained towards a magnetic field of 120 mT [14]. Dong et al. demonstrated that laminate composed of longitudinally magnetized magnetostrictive Terfenol-D and a transversely poled piezoelectric Pb(Mg\textsubscript{1/3}Nb\textsubscript{2/3})O\textsubscript{3}-PbTiO\textsubscript{3} crystal offered extremely high magnetic field sensitivity of $10^{-11}$ T [15]. Schell et al. analyzed the influence of the deposition process and heat treatment on the performance of devices to improve the limits of detection [16]. Sun et al. deposited the FeGaB film on the AlN piezoelectric materials, which enabled a measurement range of up to 300 pT in the presence of a DC-biased magnetic field [17]. Taking the magnetostriction effect, $\Delta E$ effect, and the third-order material constants into account, Yang et al. investigated the sensing mechanism of SAW magnetic field sensors [18], and they also explored a grooved sensing surface structure to improve sensitivity.

Obviously, the performance of an SAW-based current/magnetic sensor is significantly determined by the magnetostrictive coatings [19]. Terfenol-D features a larger magnetostrictive coefficient. Therefore, very high magnetic sensitivity will be expected. However, an easily oxidized nature prevents its application. Meanwhile, FeGa features lower coercivity, higher Curie temperature, lower cost, and excellent mechanical properties [20], and maximum magnetostriction coefficient is up to 400 ppm [21], which is much larger than that of Fe, Co, Ni and their alloys [22,23]. In addition, the FeGa thin film applied for microsensor and microsystem integration is conducive to the miniaturization and intelligence of the sensor, and it significantly improves the performance of the device.

In this contribution, a new design of SAW device for sensing current is proposed by employing the patterned FeGa thin film as the sensitive interface, as depicted in Figure 1. A SAW chip with a delay-line pattern was fabricated photolithographically on 128° YX LiNbO\textsubscript{3} substrate to operate at 150 MHz. To improve the sensitivity and suppress the hysteresis error, the patterned design was performed to the FeGa thin film. The proposed current sensing device was built by sputtering the FeGa thin film to the SAW chip and characterized by connecting it into the differential oscillation loops. Larger current sensitivity, low hysteresis error, excellent repeatability and stability were achieved experimentally.

![Figure 1. The scheme of patterned FeGa thin film coated SAW sensing device.](image-url)

2. Working Principle

Under the magnetic field generated by the applied current, the FeGa film produces magnetostrictive strain and so-called $\Delta E$ effect, which modulates the SAW propagation.
A layered media structure of FeGa/SiO$_2$/LiNbO$_3$ is proposed to demonstrate the sensing mechanism, as shown in Figure 2.

**Figure 2.** The layered media model (FeGa/SiO$_2$/LiNbO$_3$).

1. **In the piezoelectric media**

   The constitutive wave motion equations in a piezoelectric LiNbO$_3$ can be expressed as

   \[
   \begin{align*}
   \rho e_{xx} \frac{\partial^2 u_{I}}{\partial t^2} - c_{ijkl} \frac{\partial^2 u_{I}}{\partial x_i \partial x_j} - e_{ijkl} \frac{\partial^2 \Phi}{\partial x_i \partial x_j} &= 0 \\
   e_{ijkl} \frac{\partial^2 u_{I}}{\partial x_i \partial x_j} - \rho \frac{\partial^2 \Phi}{\partial t^2} &= 0
   \end{align*}
   \]  

   where Einstein’s summation rule is used. The indices $i, j, k, l = 1, 2, 3$, and $c, e, \rho, \lambda$ stand for the elastic, piezoelectric, dielectric constants and the mass density of the piezoelectric substrate, respectively. $u_I$ denotes the mechanical displacements, and $\Phi$ denotes the electric potential.

2. **In the SiO$_2$ media,**

   The SiO$_2$ media is considered as the isotropic and nonpiezoelectric media. Then, the acoustic wave equation can be written as

   \[
   c_{II}^{ll} \frac{\partial^2 u_{II}^{ll}}{\partial x_i \partial x_j} = \rho_a \frac{\partial^2 u_{II}^{ll}}{\partial t^2}
   \]  

   where $u_{II}^{ll}$, $c_{II}^{ll}$ and $\rho_a$ are the mechanical displacements, stiffness constants and density of the SiO$_2$ film, respectively.

3. **In the FeGa media,**

   The acoustic wave equation in the FeGa media can also be written as

   \[
   c_{III}^{III} \frac{\partial^2 u_{III}^{III}}{\partial x_i \partial x_j} = \rho_b \frac{\partial^2 u_{III}^{III}}{\partial t^2}
   \]  

   where $u_{III}^{III}$, $c_{III}^{III}$ and $\rho_b$ are the mechanical displacements, the stiffness constants and density of the FeGa film, respectively.

4. **Magnetostrictive strain of the FeGa film**

   Under the magnetic field generated by the applied current, the FeGa film produces magnetostrictive strain, which leads to changes in thickness $h$ and density $\rho_f$ of FeGa film.

   \[
   \begin{align*}
   h &= h_0(1 - \frac{1}{2}) \\
   \rho_f &= \rho_0 / [(1 + \lambda) \times (1 - \frac{1}{2}) \times (1 - \frac{1}{2})]
   \end{align*}
   \]  

   where $h_0$ and $\rho_0$ are the thickness and density of unperturbed FeGa film, respectively, and $\lambda$ is the magnetostrictive coefficient of the FeGa film.

5. **$\Delta E$ effect on the FeGa film**
The external magnetic field will also modulate the Young’s modulus \(E\) of the FeGa film, which is so-called \(\Delta \mu\) effect, and the corresponding elastic coefficients in FeGa film are expressed by the perturbed Young’s modulus \(E'\) as

\[
\begin{align*}
    c_{11} &= \frac{E' (1-\mu)}{(1+\mu)(1-2\mu)} \\
    c_{12} &= \frac{E' \mu}{(1+\mu)(1-2\mu)} \\
    c_{44} &= \frac{c_{11}-c_{12}}{2} = E'(1-2\mu)/2(1+\mu)(1-2\mu)
\end{align*}
\]

where \(\mu\) is the Poisson’s ratio.

The relationship between the electromagnetic field intensity \(H\) and current \(I\) can be described by the Biot–Savart law [24],

\[
H = \frac{\mu_0 I}{4\pi l}
\]

where \(\mu_0\) denotes the permeability in vacuum. \(l\) expresses the distance between the sensor chip and wires, which is set to 1 cm.

According to the Formulas (1)–(3), the solution of each layer media can be obtained. Then, combined with the mechanics and electrical boundary conditions, the effective surface permittivity method can be used to obtain the speed of SAW. Under the magnetic field generated by the applied current, according to the Formulas (4)–(5), the FeGa film produces magnetostrictive strain and so-called \(\Delta \mu\) effect, which modulates the SAW propagation.

The measured magnetostriction curve characteristic of FeGa is shown in Figure 3a. The simulation was done to predict the sensitivity of the proposed sensor. The parameters of LiNbO\(_3\) and SiO\(_2\) used in the simulation were consistent with the literature [11]. The mechanics and electrical boundary conditions were also the same as the literature [11]. The film thickness was set to 500 nm, and the aspect ratio was set to 1:1. The sensitivity of the proposed current sensor is calculated as \(~20.3\ \text{kHz/A}\), as shown in Figure 3b. Compared with the sensitivity of \(~11\ \text{kHz/A}\) mentioned in the literature [11], the sensitivity of the proposed sensor is increased by \(~9\ \text{kHz/A}\). The results reveal that the FeGa film can effectively improve sensor performance.

![Figure 3](image.png)

**Figure 3.** (a) The magnetostriction curve characteristic of FeGa; (b) the predicted sensitivity of the 150 MHz SAW-based current sensor.

### 3. Technical Realizations

#### 3.1. SAW Devices

LiNbO\(_3\) piezoelectric crystal features a larger electromechanical coupling coefficient \(K^2\), which benefits the reduction in insertion loss of SAW device. Therefore, 128° YX-LiNbO\(_3\) piezoelectric crystal with large \(K^2\) (5.5%) was chosen as the piezoelectric substrate of the sensing chip with a delay-line pattern, and FeGa thin film was sputtered to the SAW propagation path between the two photolithographically defined 300 nm Al transducers separated by a path length of \(~2\ \text{mm}\). Single-phase unidirectional transducers (SPUDTs)
confining the acoustic energy predominantly in one direction on the piezoelectric substrate surface were used to form the transducers to reduce the insertion loss [1]. The operation frequency was designed to 150 MHz, and the corresponding wavelength $\lambda$ was 25.84 $\mu$m. The electrode widths in SPUDTs were 3.23 $\mu$m ($\lambda/8$) and 6.46 $\mu$m ($\lambda/8$). The lengths of the input transducer and output transducer were designed to be $130\lambda$ and $40\lambda$, respectively. In addition, a comb structure was designed for the transducers to eliminate other unwanted vibration frequencies to achieve a single oscillation mode [25]. After the Al electrodes preparation, a 30 nm SiO$_2$ thin film was covered on the transducers by PECVD to protect the electrodes in FeGa deposition.

3.2. Preparation of FeGa Film

Then, the FeGa thin film was deposited onto the acoustic propagation path of the developed SAW chip to build the sensing device by employing the lift-off process. The corresponding details are described in Figure 4. Firstly, the photoresist was deposited on the prepared SAW device. Then, through a photolithography mask, the photoresist was removed in the areas, where the FeGa thin film was to be located; then, the FeGa thin film was sputtered onto the surface of the SAW chip using radio-frequency magnetron sputtering. The sputtering conditions for the base pressure, sputtering power and target-substrate distance were $1.5 \times 10^{-5}$ Pa, 100 W, and 60 mm, respectively. The Ar gas was used as the sputtering gas, and corresponding pressure was set to 1 Pa. After removed the remaining photoresist, the FeGa thin film with various patterns (dot, grating, and membrane) was formed on the SAW chip. Here, the strip width in each FeGa grating was set to $3\lambda$, and the corresponding grating spacing was set to $4\lambda$. Similarly, the length width of each FeGa dot was set to be $3\lambda \times 3\lambda$, and dot spacing in each direction was set to $4\lambda$. The developed SAW sensing devices with various FeGa thin-film patterns were pictured in Figure 5a–c.

![Figure 4. The fabrication process of FeGa film.](image)

Using the network analyzer, we characterized the developed sensing devices as shown in Figure 5f. Among them, the working frequency of the sensing devices with various FeGa patterns (dot, grating, and membranous) were measured as 150.4 MHz, 149.7 MHz, and 149.4 MHz, respectively, and their corresponding insertion losses were both less than 10 dB. The deviation in operation frequency stems from the manufacturing error, and there are almost no unacceptable effects in sensing performance.
3.3. Differential Oscillator

In this work, the oscillation loop was employed to generate the SAW chip, and the differential structure was also used to eliminate the external temperature effect, vibration noise, and magnetic noise [26–28]. The FeGa thin film coated device as the sensing chip and the naked one as the reference chip were packaged into the same metal base, and connected into the differential oscillation loop made of discrete elements as an amplifier, phase shifter, mixer, and so on (Figure 6a), and the mixed oscillation frequency signal was collected by using the frequency counter as the sensing signal.

Figure 6. (a) The view of oscillation circuit board with sensor chip; (b) the experimental setup for characterizing the SAW sensors.

4. Sensor Experiments and Discussions
4.1. Experimental Setup

The experimental setup for characterizing the developed SAW sensor is described in Figure 6b, which is composed of a Helmholtz coil system with measure range of 0–10 A, Gaussmeter, SAW sensor, frequency counter, constant current source, and constant voltage source. By varying the coil current generated by the constant current source, the Helmholz...
coil can create a varying magnetic field. The differential oscillation loop is supplied with a voltage of $+5 \text{ V}$ provided by the constant voltage source. The sensor signal is collected by the frequency counter at 60 points per minute and is plotted by the PC in real time. During the test, the SAW device was exposed to the magnetic field, and the differential oscillation loop was wrapped with aluminum foil so as to reduce the influence of the magnetic field on the circuit.

4.2. Sensor Performance Evaluation

4.2.1. Sensitivity Evaluation

First, the sensitivity of the prepared sensor was evaluated by measuring the sensing response towards increasing current values from 0 to 10 A at room temperature ($25 ^\circ \text{C}$) using the experimental setup described in Figure 6b. The effect from FeGa film thickness on sensitivity was demonstrated by measuring the sensitivity of developed sensors with various FeGa film thicknesses (300 nm, 500 nm, and 700 nm), as shown in Figure 7a. Obviously, the sensitivity increases with increasing thickness of FeGa film. This can be explained by the following formula [29]:

$$\Delta V = -f h \sum_{i=1}^{3} c_i \left( \rho - \frac{E^{(i)}}{V^2} \right)$$

where $f$, $h$, $c_i$ and $E^{(i)}$ are the operation frequency of SAW device, FeGa film thickness, coupling parameter relating to the piezoelectric substrate, and Young’s modulus of the FeGa film, respectively. It can be seen that the acoustic velocity is proportional to the film thickness when other parameters are fixed. Therefore, increasing the FeGa film thickness will improve the sensitivity. However, a turning point occurred when thicker FeGa film over 700 nm was applied. This is because the magnetic domain wall gradually changed from Neel wall to Bloch wall with the increase in the film thickness, resulting in the degradation of the film soft magnetic properties. The result indicates that too thick of a FeGa film will reduce the sensitivity. Hence, 500 nm FeGa film was chosen to construct the sensing devices in this work.

Figure 7. (a) The effects of film thickness on the sensor sensitivity; (b) the frequency response of current sensor with a 500 nm thick film.

Figure 7b shows the linear response of the proposed sensor coated with 500 nm patterned FeGa thin film. The concluded sensitivities of 37.9 kHz/A, 32.2 kHz/A, 23.1 kHz/A were obtained from the sensing devices coated with dotted, grating, and membranous FeGa thin films, respectively. The sensitivity of membranous FeGa thin film coated device approximately agreed with the predicted value. The largest sensitivity was achieved from the dotted-FeGa thin film coated device, which is the result of enlarged magnetostrictive properties and reduced coercivity in the dot-film structure [9].
4.2.2. Repeatability Test

Then, the repeatability of the 500 nm FeGa thin film coated SAW sensing device was evaluated as shown in Figure 8, which shows response profiles obtained from four consecutive 5 s on-off exposed to 10 A current at room temperature (25 °C). To evaluate the repeatability, a statistical analysis was performed to the measured results. Using the sensor response towards applied current of 10 A as a sample set (Figure 8), we evaluated repeatability by calculating the corresponding standard deviation. Usually, the standard deviation is defined by

$$\sigma = \sqrt{\frac{1}{N-1} \sum_{i=1}^{N} (x_i - \bar{x})^2}$$

(8)

where $$x_i$$, $$\bar{x}$$, and $$N$$ are the $$i$$th measurement, the average of the measurements, and the number of measurements, respectively. Hence, the standard deviations of 0.99, 0.71, and 1.13 were calculated from the sensing devices coated with dotted, grating, and membranous FeGa thin film, respectively. It can be seen that excellent reproducible runs were obtained from the prepared sensing device with various FeGa patterns. Moreover, when the current was switched from 0 A to 10 A, the frequency response of the three sensors dropped rapidly to a steady state, which means a very fast response was achieved. Moreover, sensor responses over 200 kHz towards 10 A were obtained from the sensing devices. The largest response up to 393 kHz was achieved from the sensing device coated with dotted FeGa thin film owing to its enlarging magnetostrictive properties [9].

![Figure 8. The repeatability of the proposed sensors.](image)

4.2.3. Hysteresis Measurement

Meanwhile, the hysteresis characteristics of the FeGa thin film coated SAW devices were evaluated as shown in Figure 9a. In the measurement, the applied current increased first and then decreased with a step of 1 A, and each applied current lasted for 5 s. Usually, the hysteresis error is defined by

$$\delta_H = \frac{\max(y_{ui} - y_{di})}{y_{FS}} \times 100\%$$

(9)

where the $$y_{ui}$$ and $$y_{di}$$ are the response at the same current input when the current increases and decreases, $$y_{FS}$$ is the full-scale output of the current sensor. Hence, the hysteresis errors of 0.81%, 0.92%, 2.57% were calculated from the sensing devices coated with dotted, grating, and membranous FeGa thin film, respectively. Obviously, the excellent symmetry in sensor response was observed from the dotted FeGa thin-film device. Dotted pattern releases the coercivity well and enhances the magnetostrictive strain, therefore lowering the hysteresis error significantly. This can also be demonstrated by measuring the hysteresis loops of the FeGa thin film with various patterns, as shown in Figure 9b. It indicates that lower coercivity of 61.23 Oe (Hcd) was observed from the dotted pattern over the grating (Hcg = 72.85 Oe) and the membranous pattern (Hcm = 100.17 Oe). Hence, it is reasonable to
be concluded that the dotted pattern can not only improve the detection sensitivity but also suppress the hysteresis effect effectively in magnetostrictive thin film.

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\[ \delta = \frac{y_{ui} - y_{di}}{y_{FS}} \times 100\% \]

where the \( y_{ui} \) and \( y_{di} \) are the response at the same current input when the current increases and decreases, \( y_{FS} \) is the full-scale output of the current sensor. Hence, the hysteresis errors of 0.81%, 0.92%, 2.57% were calculated from the sensing devices coated with dotted, grating, and membranous FeGa thin film, respectively. Obviously, the excellent symmetry in sensor response was observed from the dotted FeGa thin-film device. Dotted pattern releases the coercivity well and enhances the magnetostrictive strain, therefore lowering the hysteresis error significantly. This can also be demonstrated by measuring the hysteresis loops of the FeGa thin film with various patterns, as shown in Figure 9b. It indicates that lower coercivity of 61.23 Oe \((H_{cd})\) was observed from the dotted pattern over the grating \((H_{cg} = 72.85 \text{ Oe})\) and the membranous pattern \((H_{cm} = 100.17 \text{ Oe})\). Hence, it is reasonable to be concluded that the dotted pattern can not only improve the detection sensitivity but also suppress the hysteresis effect effectively in magnetostrictive thin film.

Figure 9. (a) The hysteresis of the proposed sensors; and (b) the hysteresis loop of patterned FeGa thin film.

Table 1 concludes the sensing performance of the proposed sensors with various FeGa film patterns. Obviously, the dot-patterned FeGa film coated sensing device features larger sensitivity and lower hysteresis error. Table 2 offers the sensing performance comparison of the proposed sensor in this work with the existing sensor prototype with similar structures. It is obvious that larger sensitivity was achieved from our work, and compared with the sensors coated with FeCo thin film [30], the sensitivity of the proposed sensors increases by ~77.1%. The main reason is that the FeGa thin film has a larger magnetostriction coefficient than FeCo thin film [22,23].

Table 1. The sensing performance of the proposed sensors in this work.

| SAW Sensing Devices | Magnetostrictive Film | Sensitivity (kHz/A) | Hysteresis Error |
|---------------------|----------------------|---------------------|-----------------|
| membranous-film     | FeGa                 | 23.1                | 2.57%           |
| grate-film          | FeGa                 | 32.2                | 0.92%           |
| dot-film            | FeGa                 | 37.9                | 0.81%           |

Table 2. The sensing performance comparison of the proposed sensor in this work with the existing sensor prototype with similar structures.

| Year | Material      | Frequency | Sensitivity          | Reference     |
|------|---------------|-----------|----------------------|---------------|
| 2017 | FeNi          | 150 MHz   | 10.7 kHz/A (5.35 kHz/mT) | [11]          |
| 2020 | FeCo          | 150 MHz   | 10.7 kHz/mT          | [30]          |
| 2021 | PVA bound Fe  | 433 MHz   | 678 kHz/120 mT       | [14]          |
|      | FeGa          | 150 MHz   | 37.9 kHz/A (18.95 kHz/mT) | our work     |

4.2.4. Fatigue Characteristics

Magnetostrictive strain usually leads to fatigue and aging of magnetic-sensing films. Thus, the fatigue characteristics of the FeGa thin film were investigated by cycle testing of the sensitivity of the developed sensing devices. The number of cycles was set to 100. In each cycle test, the current of 0–10 A was applied to the sensing device coated with various FeGa thin-film patterns to obtain the detection sensitivity. The cycle interval was set to 10 min. Table 3 shows the statistical analysis of the relationship between the sensor sensitivity decrease rate and the number of cycle runs. It can be seen that the sensitivity of sensors with different patterns decreased slightly with the increasing cycle runs. However, the performance decline was less than 4% after 100 cycle runs, which is
acceptable. Obviously, thanks to the good ductility and strong impact resistance of FeGa thin film itself, excellent long-time stability and weak fatigue were observed (Figure 10a), which was far better than that of the FeCo thin film [30]. Moreover, the SEM views of the FeGa thin film after 0, 50, 100 cycle testing runs are depicted in Figure 10b–d. It can be seen that the unloaded FeGa thin film was perfectly uniform. Although a few cracks appeared after 100 runs, most areas of the film remained uniform. It means excellent stability was achieved from the FeGa thin film coated sensing device in long-term runs.

Table 3. The sensitivity decrease rate after long-term runs.

| Devices          | Sensitivity Decrease Rate after Long-Term Runs |
|------------------|-----------------------------------------------|
|                  | 0     | 50    | 100   |
| membranous-film  | 0     | 2.26% | 3.6%  |
| grate-film       | 0     | 2.23% | 3.2%  |
| dot-film         | 0     | 2.93% | 3.91% |

Figure 10. (a) The fatigue measurement of developed SAW sensing devices, and the surface morphologies of the FeGa thin film in different cyclic testing runs of (b) 0, (c) 50, and (d) 100.

5. Conclusions

The SAW current sensors with different patterns of FeGa thin films were discussed. The layered media model (FeGa/SiO$_2$/LiNbO$_3$) was established to reveal the interaction between FeGa thin film and the applied external current, and the sensitivity of the sensor was simulated. The SAW devices with various FeGa thin-film patterns (dot, grating, and membranous) were designed and fabricated to improve the detection sensitivity and lower the hysteresis error. The experimental results show that the dotted FeGa thin film coated sensing devices can achieve large current sensitivity (37.9 kHz/A), low hysteresis error (0.81%), good repeatability, and weak fatigue, which is the result of enlarged magnetostrictive properties and reduced coercivity in the dot-film structure. In addition, compared with the existing sensor prototypes with similar structures, our proposed sensors perform far better. Those results indicate that the FeGa thin film with grating and dotted patterns can be
used to enhance the performance of the SAW currents sensors. Hence, the dotted FeGa thin film coated SAW current sensors have broad application prospects in the fields of current detection. The obtained results provide very encouraging results for the development of wireless passive current sensors. Meanwhile, the structure of FeGa thin film with a dotted pattern can provide a new idea for the thin-film pattern design of wireless passive current sensors.

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