W & Z Production and Asymmetries at the Tevatron

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Abstract. An overview of W and Z production in high energy hadron collisions is given. W and Z cross section and asymmetry measurements from CDF and DØ are described, with particular emphasis on recent results. The current status of precision W mass and width measurements is reported. The fundamental physics parameters that can be extracted from these measurements are described, and the relevance of W and Z production studies for the LHC is pointed out.

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1. INTRODUCTION

W and Z bosons are produced in abundance in high energy hadron collisions. Their large mass scale and well known fermion couplings make their production cross sections accurately calculable in perturbative QCD, and their leptonic decay modes provide distinctive experimental signatures that are relatively easy to identify, trigger on and separate from large backgrounds. In many respects vector boson production has become one of the most important “standard candles” in experimental hadron collider physics. At the Tevatron, measurements of W and Z inclusive cross sections are routinely used to validate detector and trigger performance and stability. Z → l⁺l⁻ events in particular, due to their negligible backgrounds and trigger redundancy as well as precisely known mass, are the most important samples for the experimental determination of energy and momentum scales and lepton identification efficiencies. Inclusive vector boson cross section measurements are necessary starting points for more detailed measurements, for example differential cross section measurements, exclusive measurements (e.g. W+n−jet), measurements of rare processes (e.g. diboson production) and precision measurements of vector boson properties. At the Large Hadron Collider (LHC) the use of massive vector bosons as standard candles may be taken one step further with their yields being used to either compute, or provide an alternative definition of, collider integrated luminosities.

In the following sections the basic physics of vector boson production at hadron colliders is reviewed, and the relevant parameters of the CDF and DØ detectors are stated. Measurements of inclusive and differential production cross sections are discussed in section 4, as well as some of the particle properties that can be extracted from these measurements. Asymmetry measurements in Z and W production are presented in section 5. Finally, the status of precision direct measurements of the W boson mass and width at the Tevatron is given in section 6.

2. MASSIVE VECTOR BOSON PRODUCTION AT HADRON COLLIDERS

Figure 1 indicates the phenomenological ingredients required for a complete description of vector boson production in hadron collisions. At leading order, a quark-antiquark pair annihilate to produce a W or Z boson, which subsequently decays to a fermion-antifermion pair. Cross sections are computed as a convolution of partial cross sections (dσ_q̅q→W/Z→ff) over parton distribution functions (PDF’s; fi(x), where x is the fraction of the proton’s momentum carried by quark flavor i):

$$\sigma_{p\bar{p}\rightarrow W/Z\rightarrow ff} = \int \sum_{i,j=u,d,s(c,b)} [f_i^q(x_p)f_j^\bar{q}(x_{\bar{p}}) + f_i^{\bar{q}}(x_p)f_j^q(x_{\bar{p}})] \times d\sigma_{q\bar{q}\rightarrow W/Z\rightarrow ff} \ dx_p \ dx_{\bar{p}}.$$ 

The longitudinal momentum (or rapidity) distribution of the produced vector bosons depends directly on the PDF’s. The rate and kinematic distributions of the decay fermions additionally depend on the couplings and branching ratios,
as well as the mass ($M_{W/Z}$) and width ($\Gamma_{W/Z}$), of the produced vector boson:

$$d\sigma_{q\bar{q} \rightarrow W/Z \rightarrow l\bar{l}}(\hat{s}, \theta_l, \phi_l) \propto \text{couplings} \times \left[ \frac{1}{(\hat{s} - M_{W/Z}^2)^2 + (\Gamma_{W/Z}\hat{s}/M_{W/Z})^2} \right],$$

where the parton-parton center of mass energy $\sqrt{\hat{s}} = E_{CM} \sqrt{x_p x_{\bar{p}}}$.

QCD corrections to this process can be divided into perturbative and non-perturbative parts. Perturbative corrections, either in the form of fixed higher order matrix elements or parton showers, modify the vector boson production kinematics - most notably the vector boson transverse momentum ($p_T$) distributions - and give rise to final states with multiple, sometimes high-$p_T$ partons. Non-perturbative effects, sometimes understood as intrinsic-$k_T$ distributions for the colliding partons, are especially important for obtaining a complete description of the low end of the vector boson $p_T$ spectra. Finally, QCD corrections modify the helicity and therefore decay angular distributions of the vector bosons, a small but measurable effect that is important to take into account for precision measurements.

By far the most important electroweak corrections to vector boson production and decay are those due to final state photon radiation from charged leptons, where the effect on lepton kinematics and identification is appreciable. Initial state radiation from the colliding quarks and, in the case of $W$ production, radiation from the $W$ itself, are important to consider in analyses of high-$p_T$ photons produced in association with a vector boson, but have a negligible impact on more inclusive $W$ and $Z$ measurements.

3. THE CDF AND DØ EXPERIMENTS AT THE TEVATRON

CDF and DØ are general purpose $\sim 4\pi$ detectors, efficiently triggering on and identifying leptonic decays of $W$ and $Z$ bosons over significant regions of phase space [1, 2]. A particular strength of the CDF detector is the excellent central tracking resolution $\delta(p_T)/p_T \approx 0.0005 \times p_T \text{ (GeV}/c) \mid |\eta| < 1 \text{, beam constrained}$. The central electromagnetic calorimeter has an energy resolution $\delta(E_T)/E_T \approx 13.5\% / \sqrt{E_T} \oplus 1.5\%$. Muon chambers cover the pseudorapidity region $|\eta| < 1$ and forward calorimeters cover the region out to $|\eta| < 3.6$, important for the accurate reconstruction of missing-$E_T$. DØ has significantly larger muon acceptance with chamber coverage and accurate momentum determination out to $|\eta| < 2$, and excellent hermeticity with calorimeter coverage out to $|\eta| < 4.2$.

The performance of the Tevatron collider continues to increase, such that at the time of this meeting is has delivered almost 1.5 fb$^{-1}$ to each experiment. The measurements presented here are based on the first $\sim 400$ pb$^{-1}$ of Run II data.

4. VECTOR BOSON PRODUCTION CROSS SECTIONS

The measurements of inclusive $W$ and $Z$ production cross-sections in leptonic decay modes provide a benchmark for all analyses of events containing high $p_T$ leptons at the Tevatron. A compilation of both Run I and Run II measurements from CDF and DØ, based on Run II datasets between 72 pb$^{-1}$ and 350 pb$^{-1}$, is shown in figure [2] where the good agreement with predictions calculated at NNLO in QCD can be observed [3].
In electron and muon decay channels, the best measurements are systematically limited at the 1–2\% level, not including an overall 6\% uncertainty on the integrated luminosity (completely correlated for all measurements from a single experiment, and partially correlated between CDF and DØ). The largest contributions to the non-luminosity systematic derive from PDF uncertainties, and residual experimental uncertainties on lepton identification efficiencies and backgrounds. Interestingly, with non-luminosity systematic uncertainties of \( \sim 2\% \), and given the uncertainty on the theoretical cross section predictions of approximately 2\%, the CDF measurements are already providing a cross check of the integrated luminosity measured for that experiment\(^1\).

The ratio of \( W \) to \( Z \) leptonic cross sections can be written as:

\[
R = \frac{\sigma_W \times BR(W \rightarrow l \nu)}{\sigma_Z \times BR(Z \rightarrow l^+ l^-)} = \frac{\sigma_W}{\sigma_Z} \cdot \frac{\Gamma_Z}{\Gamma_{\tau^+ \tau^-}} \cdot \frac{\Gamma_{W \rightarrow l \nu}}{\Gamma_W}.
\]

With the ratio of inclusive production cross sections taken from a NNLO calculation, the measurement of the \( Z \) leptonic branching ratio from LEP and a Standard Model calculation of the \( W \) leptonic decay partial width, a measurement of \( R \) can therefore be interpreted as an indirect determination of the full \( W \) decay width. The CDF 72 pb\(^{-1}\) analysis results in a measurement \( \Gamma_W = 2.092 \pm 0.042 \) GeV that is already comparable in precision with the world average result. Analyses are currently being developed with the goal of minimizing the systematic uncertainty on the cross section ratio rather than the individual \( W \) and \( Z \) cross sections, in order to further improve the indirect \( W \) width determination.

Tau decay modes of \( W \) and \( Z \) bosons are experimentally much more challenging in many respects, including triggering, identification and separation from backgrounds. However the physics reward is significant, allowing tests of 3\(^{rd}\) generation lepton universality and establishing a benchmark for many searches, most notably the search for the MSSM Higgs bosons. Both CDF and DØ have recently performed cross section measurements for \( Z \rightarrow \tau^+ \tau^- \) production, where one \( \tau \) decays leptonically and the other hadronically \(^4\). The reconstruction of the hadronic tau decay modes involves combining information from both the tracking and calorimetry, with constraints from the tau mass and decay topologies. Figure 3 shows the mass distributions from the two analyses, showing good agreement with Monte Carlo after applying background corrections. The corresponding cross sections:

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\begin{align*}
\sigma_Z \times BR(Z \rightarrow \tau^+ \tau^-) &= 237 \pm 15 \text{ (stat.)} \pm 18 \text{ (syst.)} \pm 15 \text{ (lum.) pb} \quad \text{(DØ; 226 pb\(^{-1}\))} \\
\sigma_Z \times BR(Z \rightarrow \tau^+ \tau^-) &= 265 \pm 20 \text{ (stat.)} \pm 21 \text{ (syst.)} \pm 15 \text{ (lum.) pb} \quad \text{(CDF; 350 pb\(^{-1}\))}
\end{align*}
\]

agree very well with measurements in the electron and muon channels. In addition CDF have a measurement of the \( W \) production cross section in the hadronic tau decay channel using 72 pb\(^{-1}\), and a corresponding determination of the ratio \( BR(W \rightarrow \nu \tau)/BR(W \rightarrow e \nu) = 0.99 \pm 0.04 \text{ (stat.)} \pm 0.07 \text{ (syst.)} \). An improved measurement of this ratio with much higher integrated luminosity will be particularly interesting to compare to measurements from LEP II.

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\( ^1 \) Integrated luminosity corrections for the DØ experiment are currently being re-evaluated.
4.1. Differential Cross Sections

CDF and DØ have moved on from inclusive cross sections to the measurement of differential cross sections. Measuring the Drell-Yan cross section $d\sigma_{l^+l^-}/dM$ over as large a mass range as possible controls an important background to searches for new physics in dilepton channels. Both the mass and the rapidity $Y$ differential cross section $d\sigma_{l^+l^-}/dY$ can, with sufficient integrated luminosity, be used to constrain PDFs and test higher-order QCD. Figure 4 shows measured Drell-Yan mass ($Z$ boson rapidity) differential cross sections in muon (electron) channels from CDF (DØ), both with 337 pb$^{-1}$ of data. The agreement with theoretical predictions, after careful unfolding of the data for smearing effects, is very good.

Differential cross section measurements for $W$’s are harder than for $Z$ bosons, due to the incomplete kinematic reconstruction of events with neutrinos in the final state. As a first attempt, the CDF experiment has measured the cross section for $W$ production with forward electrons ($1.2 \leq |\eta_e| \leq 2.8$) in 223 pb$^{-1}$ of data, using silicon-only small angle tracking and with a different triggering strategy to central leptons. The ratio of central to forward $W$ cross sections is particularly interesting:

$$R_{\text{central}/\text{forward}}^{\text{CDF}} = 0.925 \pm 0.033.$$  

The prediction for this ratio depends on the choice of PDF set:

$$R_{\text{central}/\text{forward}}^{\text{CTEQ 6.1}} = 0.924 \pm 0.037, \quad R_{\text{central}/\text{forward}}^{\text{MRST 01E}} = 0.941 \pm 0.012.$$  

Although not yet significant, there is clearly hope that with more data, this and other differential cross section measurements at the Tevatron can yield useful inputs to global PDF fits.

5. ASYMMETRIES

In addition to cross sections, measured asymmetries are particularly useful for the extraction of underlying physics parameters such as electroweak couplings and PDF’s. Many systematics cancel in the measurement of asymmetries as opposed to absolute cross sections, and in certain cases (most notably the search for $Z'$ bosons), hints of new or unexpected physics may first turn up as asymmetry rather than rate anomalies.

$^2$ The rapidity $Y$ is a function of energy and longitudinal momentum: $Y = \frac{1}{2} \ln \left( \frac{E+p_z}{E-p_z} \right)$.
FIGURE 4. (left) The differential cross section for dimuon pairs as a function of dimuon mass from CDF, normalized to the Z pole cross section. Note the good agreement between data and theory over four orders of magnitude in cross section. (right) The unit normalized differential cross section for Z production as a function of vector boson rapidity, measured by DØ in the electron channel.

The Drell-Yan forward-backward asymmetry compares the fractions of events for which the negatively charged lepton is produced in the forward and backward hemispheres, defined in the parton-parton center of mass system:

$$A_{FB} = \frac{\sigma_F - \sigma_B}{\sigma_F + \sigma_B}, \quad \text{where} \quad \sigma_{F(B)} = \int_{(0)}^{(1)} \frac{d\sigma}{d\cos \theta^*} d\cos \theta^*.$$  

The result of a recent CDF update to their published $A_{FB}$ analysis \[5\] is shown in figure 5. The structure around the Z pole, as well as the measured asymmetry at high mass where indications of new physics may first be expected to be observed, agree well with theoretical predictions. The previous analysis has also used the measured asymmetry to place constrains on the neutral current light quark couplings. Although less precise, the Tevatron $A_{FB}$ data, along with data from the analysis of deep inelastic scattering at HERA, do break a degeneracy in the determination of light quark couplings at LEP, providing an important confirmation of the Standard Model.

The observed W charge asymmetry, defined with respect to the decay lepton direction, is a combined effect of both the underlying W production asymmetry and $(V-A)$ decay asymmetry:

$$A(\eta_l) = \frac{\frac{d\sigma_{+}}{d\eta_l} - \frac{d\sigma_{-}}{d\eta_l}}{\frac{d\sigma_{+}}{d\eta_l} + \frac{d\sigma_{-}}{d\eta_l}} = A(y_W) \otimes (V-A).$$

The expected W charge asymmetry is sensitive to the assumed PDF, in particular the $(d/u)$ ratio at high-$x$, and benefits from increased statistics with respect to the Z rapidity measurement. Important experimental issues are forward lepton identification and, crucially, well controlled charge mis-identification rates in order to correct the observed asymmetry for any dilution due to lepton charge mis-assignment. Figure 5 shows a recent W charge asymmetry measurement by DØ in the muon channel, where charge mis-identification rates were kept at the $10^{-4}$ level out to muon pseudorapidities of 2. Interestingly, the measurement uncertainties are now appreciably smaller than the variation in theoretical predictions that can be generated by varying the input PDF set. This indicates that this data would already contribute additional constraining power to future global PDF fits. CDF have measured the asymmetry using electrons in a smaller dataset \[6\]. They have additionally shown that certain lepton kinematic regions are more sensitive to PDF variations than others. Analyses are currently underway to fully exploit all the kinematic information available in W events with the goal of unfolding directly back to the underlying W production asymmetry.

6. PRECISION MEASUREMENTS OF THE W MASS AND WIDTH

The precision determination of the W mass is one of the most important measurements to be performed at the Tevatron. $M_W$ is a critical input to Standard Model fits which can constrain the mass of the unobserved Higgs boson or, subsequent to a discovery of a Higgs boson, may give indications as to what lies beyond the Standard Model.
The width of the $W$ is a less sensitive observable in global electroweak fits, but the direct measurement of the $W$ width nevertheless confirms a basic prediction of the Standard Model and provides a useful cross check of indirect measurements.

The most precise top mass measurements at the Tevatron are at the level of 1%. By contrast the goal for the $M_W$ is a measurement substantially better than 0.1%. This highlights the extremely difficult nature of this measurement, requiring exquisite understanding of $W$ production and decay, detector response and the effect of backgrounds. CDF have estimated that in the first 200 $pb^{-1}$ of Run II data, they will measure the $W$ mass with a precision of at least 76 MeV, better than the combined Tevatron Run I uncertainty. DØ have started with a direct measurement of the $W$ width in 177 $pb^{-1}$ of Run II data: $\Gamma_W = 2.011 \pm 0.093 \text{ (stat.)} \pm 0.107 \text{ (syst.)} \text{ GeV}$. Both experiments are finalizing new measurements of the $W$ mass, with an ultimate goal for Run II of $30 - 40$ MeV per experiment.

7. CONCLUSIONS

The CDF and DØ experiments have completed benchmark measurements of inclusive $W$ and $Z$ production, as well as differential cross section and asymmetry measurements. These measurements are providing important information on fundamental $W$ and $Z$ properties, as well as parton distribution functions and other aspects of vector boson production physics. With the basic signatures and experimental techniques involved in the measurement of $W$ and $Z$ production well understood, attention is now focused on optimizing analyses for sensitivity to PDF’s and other physics parameters of interest. All of this information is being brought to bear in the precision measurement of the $W$ mass in Run II, the first results on which are expected soon.

Ultimately, measurements of $W$ and $Z$ production at the Tevatron will be used as inputs to the accurate modeling of vector boson production at the LHC, crucial for using these processes to help commission and calibrate LHC detectors. In general, vector boson production promises to continue to be one of the most useful standard candles of hadron collider physics.

REFERENCES

1. D. Acosta et al. (CDF Collaboration), Phys. Rev. D 71, 032001 (2005).
2. V. M. Abazov et al. (DØ Collaboration), "The Upgraded DØ Detector", hep-physics/0507191 (submitted to Nucl. Instrum. Methods Phys. Res. A).
3. D. Acosta et al. (CDF Collaboration), Phys. Rev. Lett. 94, 091803 (2005); hep-ex/0508029 (submitted to Phys. Rev. D).
4. V. M. Abazov et al. (DØ Collaboration), Phys. Rev. D 71, 072004 (2005); A. Safonov (for the CDF Collaboration), Nucl. Phys. Proc. Suppl. 144 323 (2005);
5. D. Acosta et al. (CDF Collaboration), Phys. Rev. D 71, 052002 (2005).
6. D. Acosta et al. (CDF Collaboration), Phys. Rev. D 71, 051104(R) (2005).