Research on Power Quality Disturbance Detection Method Based on Improved Ensemble Empirical Mode Decomposition

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Abstract: With the increasing proportion of various unbalanced loads in the power grid, power quality is seriously challenged. It is of great significance to effectively detect, analyze, and evaluate the power quality problems. First, this paper introduces the current situation of power quality (PQ) disturbance detection methods. It summarizes that the current PQ disturbance detection methods include Wavelet Transform (WT), Hilbert–Huang Transform (HHT), and Ensemble Empirical Mode Decomposition (EEMD). EEMD has a better detection accuracy, but its running time is longer. Therefore, to reduce the running time of the EEMD algorithm, this paper proposed two improvements: increasing the screening threshold and selecting piecewise cubic Hermite interpolation polynomial fitting. At the same time, the mathematical models of transient power quality disturbance and harmonic were established for comparative verification. The experimental results showed that the improved Ensemble Empirical Mode Decomposition (IEEMD) algorithm greatly reduced the running time of the algorithm on the premise of ensuring the detection accuracy. Hence, the improvement of this paper is of great significance for the industrial application of the EEMD algorithm.

Keywords: power quality; improved ensemble empirical mode decomposition; Hilbert–Huang transform; running time

1. Introduction

In the modern power system, power quality has become very unstable due to the large numbers of nonlinear loads and generators in the grid. Notably, power electronic-based systems such as adjustable speed drives, power supplies for IT-equipment, high-efficiency lighting, and inverters in systems generating electricity from distributed renewable energy sources are sources of disturbances [1]. The power quality (PQ) not only affects the operation of the power system, but it is closely related to the development of the national economy. High-quality power can effectively make all parts of the power system to run efficiently and smoothly, allowing the national economy to develop at high speed. On the contrary, the cost of the power industry will increase significantly and may lead to the deterioration of the stability of the power system, which will seriously affect the national economy. Hence, it is necessary to improve the PQ.

Accurate detection of power quality disturbances is a prerequisite for improving power quality problems. Since the 1980s, researchers have proposed several detection methods [2]. This paper mainly studies the Ensemble Empirical Mode Decomposition (EEMD) algorithm and proposes improvements. The EEMD algorithm adds white noise to the signal, and then decomposes it by Empirical Mode Decomposition (EMD), and uses the filtering characteristics of white noise to suppress the mode aliasing [3]. At present, several researchers have proposed the improvement of the EEMD algorithm.
In Reference [4], the Independent Component Analysis algorithm (ICA) was combined with EEMD to ensure the orthogonality and independence of the decomposed IMF to eliminate redundancy, effectively solving the noise reduction problem and accurately extracting the signal features. In Reference [5], the auxiliary positive and negative white noise was added to the original signal, which effectively eliminated the residual auxiliary noise of the reconstructed signal. Still, the amount of calculation was further increased, which was contrary to the aging of detection. In Reference [6], comparing EMD and EEMD, EMD followed the median filter and eliminated the impulse noise in the IMF, which could significantly improve the ability to distinguish the signal feature. In Reference [7], a method based on Complementary Ensemble Empirical Mode Decomposition (CEEMD) and Singular Spectrum Analysis (SSA) was proposed, which could effectively suppress strong noise and extract weak fault features, although it took a long time.

First, this paper introduces several common PQ detection methods, such as the Hilbert-Huang Transform (HHT) and EEMD algorithm. Second, it analyzes its shortcomings and proposes an improved EEMD algorithm from the algorithm running time. Third, it establishes several PQ disturbance mathematical models, obtains the detection results of the above methods through simulation experiments, analyzes and compares their advantages and disadvantages, and finally summarizes and prospects the full text.

2. Methodologies

2.1. Hilbert–Huang Transform (HHT)

HHT is a signal processing method proposed by Huang et al. in 1998 to have strong processing and decomposition capabilities for nonlinear and non-stationary signals [8]. It mainly includes the EMD [3] algorithm and Hilbert transform.

2.2. Ensemble Empirical Mode Decomposition (EEMD)

Huang and Flandrin proposed the EEMD algorithm for the mode mixing in the EMD [9,10] method and the characteristics of the white noise decomposition process [3]. The specific decomposition steps are as follows.

1. Add a set of white noise \( \omega(t) \) to the original signal \( x(t) \) to get an overall signal \( X(t) \):

\[
X(t) = x(t) + \omega(t)
\]

2. Use EMD to decompose the original sequence \( X(t) \) after adding white noise to get \( n \) decomposed natural modal components \( c_{ij}(t) \) and a residual component \( r_{in}(t) \). This manuscript sets \( c_{ij}(t) \) as EMDIMF.

\[
X(t) = r_{in}(t) + \sum_{j=1}^{n} c_{ij}(t)
\]

3. Repeat the above two steps for a total of \( N \) times, the amplitude of the white noise sequence added each time is different. \( X_i(t) \) obtained by adding white noise to the original sequence \( x(t) \) and the EMDIMF obtained by the \( i \)-th decomposition is \( c_{ij}(t) \), the resulting margin is \( r_{in}(t) \).

\[
X_i(t) = r_{in}(t) + \sum_{j=1}^{n} c_{ij}(t)
\]

4. \( c_{ij}(t) \) is obtained by \( c_{ij}(t) \) taking the overall average, Let \( c_{ij}(t) \) be the IMF in this manuscript

\[
c_{ij}(t) = \frac{1}{N} \sum_{j=1}^{n} c_{ij}(t)
\]
(5) Reconstruct $x(t)$ with each IMF component and the final remaining amount:

$$x(t) = \sum_{j=1}^{n} c_{ij}(t) + r_n(t) \quad (5)$$

The white noise sequence added in the above steps should obey the normal distribution of $(0, (\alpha \varepsilon)^2)$, where $\alpha$ is the intensity parameter of the noise, and $\varepsilon$ is the standard deviation of the signal.

2.3. Improved Ensemble Empirical Mode Decomposition (IEEMD) Method

The EEMD algorithm in Section 2.2 solves the mode mixing problem of the EMD algorithm, but it also leads to a severe drawback, i.e., its operation for a long time. To improve the running speed and not affect the accuracy of power quality detection, we chose to improve the EEMD algorithm from two aspects: algorithm running time and envelope fitting effect. The specific flow chart is shown in Figure 1.

2.3.1. Algorithm Runtime Improvement

Usually, to reduce the running time of the program, we can reduce the number of loops of the algorithm. In the EEMD algorithm, when white noise is added to obtain the IMF components of each order, the problem of how to screen out the IMF is involved. The traditional EEMD method takes the standard deviation of two consecutive screening components as the measurement standard. Whether the screening process ends is judged by comparing it with the screening threshold. Therefore, this paper chose to increase the screening threshold appropriately without affecting the detection accuracy, thereby reducing the number of cycles, reducing the running time, and speeding up detection.
2.3.2. Envelope Fitting Improvement

The EEMD algorithm still has problems such as envelope fitting and endpoint effects. Therefore, to ensure that the screening threshold is increased while maintaining the detection accuracy, this paper chose to improve the envelope fitting.

The cubic spline method is used for envelope fitting. However, we found that the piecewise cubic Hermite Interpolation Polynomial (PCHIP) method fits the signal closer to the original signal. The two methods construct the envelope in the same way, but the method of selecting the slope is different. In general, when the data is smooth, the results obtained by spline are more accurate. When the data is not smooth, the PCHIP fit is better than a spline. Take the voltage swell as an example. Figure 2 shows the comparison result.

![Figure 2. Voltage swell signal upper (a) and lower (b) envelopes.](image)

3. Disturbances Models

The literature addresses the modeling of PQ disturbances to verify the various detection methods in Section 2, and a series of efficient modeling algorithms have been proposed [11–14]. The unified setting of the disturbance start time is 0.07 s, and the end time is 0.14 s (pulse transient start time is 0.0996 and end time is 0.1004). The PQ disturbance signal generation models and their control parameters are shown in Table 1.

| Label | Disturbance Class      | Modeling Equations                                                                 | Equations’ Parameters |
|-------|------------------------|------------------------------------------------------------------------------------|-----------------------|
| C0    | Pule Signal            | $h(t) = A \cos(\omega t)$                                                       | $A = 1(\text{pu}), f = 50\text{Hz}, \omega = 2\pi f$ |
| C1    | Voltage Sag            | $h(t) = A[1 - k[u(t_1) - u(t_2)]] \cos(\omega t)$                                | $0.1 < k < 0.9, 0.5T \leq t_2 - t_1 \leq 9T$ |
| C2    | Voltage Swell          | $h(t) = A[1 + k[u(t_1) - u(t_2)]] \cos(\omega t)$                                | $0.1 < k < 0.9, 0.5T \leq t_2 - t_1 \leq 9T$ |
| C3    | Voltage Interruption   | $h(t) = A[1 - k[u(t_1) - u(t_2)]] \cos(\omega t)$                                | $0.9 < k < 1.0, 0.5T \leq t_2 - t_1 \leq 9T$ |
| C4    | Oscillatory Transient  | $h(t) = A[\cos(\omega t) + ke^{-b\Delta t(h_1-t_2)} \cos(\omega t)]u(t_1) - u(t_2)]$ | $k = 0.3, b = 0.6, c = 7$ |
| C5    | Impulsive Transient    | $h(t) = A[\cos(\omega t) + b[u(t_1) - u(t_2)]]$                                  | $b = 0.6, 0 < t_2 - t_1 < 3\text{ms}$ |
| C6    | Harmonic               | $h(t) = A \sin(\omega t) + \alpha_3(3\omega t) + \alpha_5(5\omega t) + \alpha_7(7\omega t)$ | $0.02 < \alpha_3, \alpha_5, \alpha_7 < 0.1$ |

4. Experimentation and Results

All experiments in this manuscript are in Windows 10, equipped with 2.50 GHz, Intel (R) corei7-6500U CPU, and a 12 GB RAM. All simulation experiments were carried out with MATLAB R2018a (The MathWorks, Inc., Natick, MA, USA).

4.1. PQ Detection Based on EMD

The difference between EMD and EEMD is that the EMD does not add white noise to the original signal, but directly decomposes the original signal to obtain the IMF component. Therefore, there is a specific mode mixing phenomenon, which needs to be screened and judged to obtain a clear IMF.
component. Through the literature review, we found that the first IMF component $c_1(t)$ does not have a modal mixing phenomenon. Thus, only the Hilbert transform is performed on $c_1(t)$ to obtain the instantaneous frequency of the signal, and the detection results are shown in Figures 3–8.

Figure 3. Voltage swell IMF components (a), margin (b), and frequency parameter (c).

Figure 4. Voltage sag IMF components (a), margin (b), and frequency parameter (c).
Figure 3. Voltage swell IMF components (a), margin (b), and frequency parameter (c).

Figure 4. Voltage sag IMF components (a), margin (b), and frequency parameter (c).

Figure 5. Voltage interruption IMF components (a), margin (b), and frequency parameter (c).

Figure 6. Oscillatory transient IMF components (a), margin (b), and frequency parameter (c).
Figure 7. Impulsive transient IMF components (a), margin (b), and frequency parameter (c).

Figure 8. Harmonic IMF components (a), margin (b), and frequency parameter (c).
4.2. PQ Detection Based on EEMD

The test results based on the EEMD algorithm are shown in Figures 9–14. Based on the suggestions of Huang et al. [3], not all IMF components were required for detection and analysis, so it was necessary to select and determine appropriate IMF components to express the physical meaning of signals. In this detection, the first six IMF components were selected for analysis, and the third IMF component was selected for the Hilbert transform to get the amplitude and frequency of the signal. For voltage swell, voltage sag, and voltage interruption, the integrated average number N was 110, and the noise standard deviation was 0.05. For the oscillatory transient, the N was 105, and the noise amplitude standard deviation was 0.06. For the impulsive transient, the N was 105, and the noise amplitude standard deviation was 0.08. For the harmonic, the N was 105, and the noise amplitude standard deviation was 0.15.

![Image of voltage swell IMF components, amplitude, and frequency](image_url)

*Figure 9. Voltage swell IMF components (a), amplitude (b), and frequency (c).*
Figure 9. Voltage swell IMF components (a), amplitude (b), and frequency (c).

Figure 10. Voltage sag IMF components (a), amplitude (b), and frequency (c).

Figure 11. Voltage interruption IMF components (a), amplitude (b), and frequency (c).

Figure 12. Oscillatory transient IMF components (a), amplitude (b), and frequency (c).
Figure 11. Voltage interruption IMF components (a), amplitude (b), and frequency (c).

Figure 12. Oscillatory transient IMF components (a), amplitude (b), and frequency (c).

Figure 13. Impulsive transient IMF components (a), amplitude (b), and frequency (c).

Figure 14. Harmonic IMF components (a), amplitude (b), and frequency (c).
4.3. PQ Detection Based on Improved EEMD

Based on the improved EEMD, PQ disturbance detection was similar to Section 4.2. The first six IMF components were selected for analysis, and the third IMF component was selected for the Hilbert transformation to obtain the signal amplitude and frequency. The detection results are shown in Figures 15–20. For voltage swell, voltage sag, and voltage interruption, the integrated average number N was 110, and the noise standard deviation was 0.03. For the oscillatory transient, the N was 105, and the noise amplitude standard deviation was 0.20. For the impulsive transient, the N was 105, and the noise amplitude standard deviation was 0.05. For the harmonic, the N was 105, and the noise amplitude standard deviation was 0.14.
Figure 13. Impulsive transient IMF components (a), amplitude (b), and frequency (c).

Figure 14. Harmonic IMF components (a), amplitude (b), and frequency (c).

Figure 15. Voltage swell IMF components (a), amplitude (b), and frequency (c).

Figure 16. Voltage sag IMF components (a), amplitude (b), and frequency (c).
Figure 17. Voltage interruption IMF components (a), amplitude (b), and frequency (c).

Figure 18. Oscillatory transient IMF components (a), amplitude (b), and frequency (c).
4.4. PQ Detection Based on Wavelet Transform (WT)

To analyze the advantages and disadvantages of the improved EEMD method more objectively, we chose the WT [14–17] as a comparison group. The test results are shown in Figures 21–26. In general, the starting and ending time of PQ disturbances can be obtained by observing and analyzing the changes in $d_1$ in Figures 21–26.

**Figure 18.** Oscillatory transient IMF components (a), amplitude (b), and frequency (c).

**Figure 19.** Impulsive transient IMF components (a), amplitude (b), and frequency (c).

**Figure 20.** Harmonic IMF components (a), amplitude (b), and frequency (c).
4.4. PQ Detection Based on Wavelet Transform (WT)

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Figure 21. Voltage swell.

Figure 22. Voltage sag.

Figure 23. Voltage interruption.
5. Discussion

In this paper, the detection time point and the algorithm run-time were taken as the comparison standard. The comparison of the detection results of the four methods is shown in Tables 2–6.
Table 2. The test results of the disturbances start time point.

| Detection Method | Swell | Voltage Sag | Interruption | Oscillation Transient | Pulse Transient | Harmonic |
|------------------|-------|-------------|--------------|-----------------------|----------------|----------|
| EMD              | 0.0694| 0.0696      | 0.0696       | 0.0698                | 0.0992         | 0.0698   |
| EEMD             | 0.0696| 0.0699      | 0.0700       | 0.0698                | 0.0994         | 0.0696   |
| IEEMD            | 0.0696| 0.0698      | 0.0700       | 0.0698                | 0.0994         | 0.0700   |
| WT               | 0.0702| 0.0704      | 0.0701       | 0.0690                | 0.0978         | 0.0701   |
| Actual time      | 0.0700| 0.0700      | 0.0700       | 0.0700                | 0.0996         | 0.0700   |

Table 3. The test results of the disturbances end time point.

| Detection Method | Swell | Voltage Sag | Interruption | Oscillation Transient | Pulse Transient | Harmonic |
|------------------|-------|-------------|--------------|-----------------------|----------------|----------|
| EMD              | 0.1396| 0.1394      | 0.1398       | 0.1392                | 0.1006         | 0.1398   |
| EEMD             | 0.1398| 0.1396      | 0.1400       | 0.1396                | 0.1004         | 0.1401   |
| IEEMD            | 0.1398| 0.1396      | 0.1400       | 0.1402                | 0.1004         | 0.1401   |
| WT               | 0.1401| 0.1401      | 0.1402       | 0.1416                | 0.1020         | 0.1412   |
| Actual time      | 0.1400| 0.1400      | 0.1400       | 0.1400                | 0.1004         | 0.1400   |

Table 4. The relative error of the disturbances start time point.

| Detection Method | Swell | Voltage Sag | Interruption | Oscillation Transient | Pulse Transient | Harmonic |
|------------------|-------|-------------|--------------|-----------------------|----------------|----------|
| EMD              | −0.85%| −0.57%      | −0.57%       | −0.29%                | −0.40%         | −0.29%   |
| EEMD             | −0.57%| −0.14%      | 0            | −0.29%                | −0.20%         | −0.29%   |
| IEEMD            | −0.57%| −0.29%      | 0            | −0.29%                | −0.20%         | 0        |
| WT               | +0.29%| +0.57%      | +0.14%       | +1.43%                | −1.81%         | +14%     |

Table 5. The relative error of the disturbances end time point.

| Detection Method | Swell | Voltage Sag | Interruption | Oscillation Transient | Pulse Transient | Harmonic |
|------------------|-------|-------------|--------------|-----------------------|----------------|----------|
| EMD              | −0.29%| −0.42%      | −0.14%       | −0.57%                | +0.20%         | −0.14%   |
| EEMD             | −0.14%| −0.29%      | 0            | −0.29%                | 0              | +0.07%   |
| IEEMD            | −0.14%| −0.29%      | 0            | +0.14%                | 0              | +0.07%   |
| WT               | +0.07%| +0.07%      | +0.14%       | 1.43%                 | +1.59%         | +0.86%   |

Table 6. The running time of the detection methods.

| Running Time | Swell | Voltage Sag | Interruption | Oscillation Transient | Pulse Transient | Harmonic |
|--------------|-------|-------------|--------------|-----------------------|----------------|----------|
| EMD          | 0.6051| 0.5415      | 0.5986       | 0.5876                | 0.5580         | 0.1713   |
| EEMD         | 6.7108| 6.3397      | 4.3448       | 5.4248                | 4.4122         | 4.8157   |
| IEEMD        | 0.9805| 1.4137      | 1.4682       | 2.1862                | 2.1515         | 2.0306   |
| WT           | 0.6988| 0.8136      | 0.6760       | 0.8385                | 0.7086         | 0.6972   |

5.1. Time Point Accuracy

The detection results of the four detection methods for the disturbance start and stop time are summarized and compared with the actual results, as shown in Tables 2 and 3.

To more intuitively explain the accuracy of the detection method, we compared the start and end time of the disturbance obtained by the four detection methods to the actual time. The relative error of the obtained results is calculated to obtain Tables 4–6.

Table 5 shows that compared to the EMD algorithm and the WT, the relative errors of the EEMD algorithm and the improved EEMD method for detecting the start and end time of the disturbance
and the start and end time of the actual disturbance are generally small. It could be seen from the comparison results that the relative error of the improved EEMD algorithm and the traditional EEMD algorithm was almost equal. This result indicated that the improved EEMD algorithm ensured that the accuracy of the detection time point was consistent with the traditional EEMD algorithm.

5.2. Algorithm Running Time

This paper used MATLAB's tic/toc method to calculate the time used for several detection methods. The running time of the four detection methods is shown in Table 6.

By comparing and analyzing the data in the table, we found that the running time difference between the improved EEMD algorithm and the WT method was about 0.3s. Still, the detection accuracy of this paper was higher than the WT method. Compared to the EEMD, the running time of the improved EEMD method was reduced significantly, and the running time was saved by nearly 6s, which was only 14.61% of the running time of the traditional EEMD. The results showed that the improved EEMD was significantly better than the traditional EEMD in terms of the algorithm running speed.

6. Conclusions

This paper mainly focuses on the problem that the EEMD algorithm is applied to power quality disturbance detections when the running time is too long. We proposed an improved method for ensuring the detection accuracy and reducing the duration of the EEMD algorithm. Concurrently, to objectively and dialectically analyze the advantages and disadvantages of the improved EEMD method, the detection results are compared with the EMD, EEMD, and WT. This proved that the improved EEMD algorithm dramatically reduced the operation time of the algorithm on the premise of ensuring the high accuracy of detection time. Of course, there are still some shortcomings in this paper, mainly because the EEMD algorithm lacks specific adaptability and needs further thinking. At the same time, the disturbance signals proposed in the example simulation of this paper are too ideal and straightforward, and there is a particular gap with the actual field data. Next, we will verify a large amount of field data and continually modify the algorithm.

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Abbreviations

| Abbreviation | Definition                        |
|--------------|----------------------------------|
| PQ           | Power Quality                    |
| WT           | Wavelet Transform                |
| HHT          | Hilbert-Huang Transform          |
| EMD          | Empirical Mode Decomposition     |
| EEMD         | Ensemble Empirical Mode Decomposition |
| IMF          | Intrinsic Mode Function          |
| IEEEMD       | Improved Ensemble Empirical Mode Decomposition |
| PCHIP        | Piecewise Cubic Hermite Interpolation Polynomial |
| SSA          | Singular Spectrum Analysis       |
| CEEMD        | Complementary Ensemble Empirical Mode Decomposition |
| ICA          | Independent Component Analysis algorithm |
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