Testing *ab initio* nuclear structure in neutron-rich nuclei: lifetime measurements of second $2^+$ states in $^{16}$C and $^{20}$O.

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To test the predictive power of *ab initio* nuclear structure theory, the lifetime of the second $2^+$ state in neutron-rich $^{20}$O, $\tau(2^+) = 150^{+80}_{-30}$ fs, and an estimate for the lifetime of the second $2^+$ state
in $^{16}$C have been obtained, for the first time. The results were achieved via a novel Monte Carlo technique that allowed us to measure nuclear state lifetimes in the tens-to-hundreds femtoseconds range, by analyzing the Doppler-shifted $\gamma$-transition line shapes of products of low-energy transfer and deep-inelastic processes in the reaction $^{18}$O (7.0 MeV/u) + $^{185}$Ta. The requested sensitivity could only be reached owing to the excellent performances of the AGATA $\gamma$-tracking array, coupled to the PARIS scintillator array and to the VAMOS++ magnetic spectrometer. The experimental lifetimes agree with predictions of $ab\ initio$ calculations using two- and three-nucleon interactions, obtained with the valence-space in-medium similarity renormalization group for $^{20}$O, and with the no-core shell model for $^{16}$C. The present measurement shows the power of electromagnetic observables, determined with high-precision $\gamma$ spectroscopy, to assess the quality of first-principles nuclear structure calculations, complementing common benchmarks based on nuclear energies. The proposed experimental approach will be essential for short lifetimes measurements in unexplored regions of the nuclear chart, including r-process nuclei, when intense ISOL-type beams become available.

Atomic nuclei are composed of protons and neutrons, which, in turn, are systems of quarks and gluons confined via the strong interaction, as described by Quantum Chromodynamics (QCD). Ideally, one would like to obtain the properties of nuclei solving QCD, but despite recent progress this is beyond current computational capabilities [1–3]. At the energy and momentum scales relevant for nuclear structure, chiral effective field theory (EFT), an effective theory based on the symmetries of QCD, provides a practical alternative [4–6]. In chiral EFT the degrees of freedom are nucleons and pions, and nuclear forces are given by a systematic expansion of two- (NN), three- (3N) and many-nucleon interactions that includes pion exchanges and contact terms.

In recent years, chiral EFT interactions have been combined with $ab\ initio$ approaches that consider all nucleons in the solution of the nuclear many-body problem, in studies of mid-mass nuclei up to tin [7–12]. Theoretical results are typically compared to the simplest experimental observables, namely binding and excitation energies. First calculations of medium-mass nuclei with chiral NN+3N interactions predicted correctly the oxygen neutron dripline at $^{20}$O [8, 13], and later works reproduced well the excitation spectra of neutron-rich oxygen isotopes [8]. In neutron-rich calcium and nickel isotopes, the shell evolution was also satisfactorily predicted [14–16]. Tests of $ab\ initio$ calculations against other observables include charge radii [17, 18], beta decay lifetimes [19], and elastic proton scattering off $^{10}$C [20]. Electromagnetic (EM) responses have also been studied in selected nuclei [21–24]. A general agreement between theory and experiment was found.

Electric and magnetic $\gamma$ decays provide a more demanding, complementary test of theoretical approaches. So far, EM decays in light/medium-mass systems have only been explored in few cases [24–29]. In contrast to energies or beta decays, $ab\ initio$ methods do not yet consistently describe all the data related to EM transitions. This calls for precision measurements of EM observables which are sensitive to the details of the calculations. Ideal cases are neutron-rich O and C isotopes. Here, $ab\ initio$ approaches show a strong sensitivity of EM decays to 3N forces which significantly affect the lifetime of selected excited states, by changing the wave function composition [30].

In this paper, we focus on the lifetime determination of the second $2^+$ excitations, $2^+_2$, in $^{20}$O and $^{16}$C nuclei. We confront our results with predictions of the valence-space in-medium similarity renormalization group (VS-IMSRG) and of the no-core shell model (NCSM) of Ref. [30], both including NN and 3N forces. Previous experiments have only set limits on the lifetime of these $2^+_2$ states, of the order of a few ps, and provided information on branching ratios in their decays [31–34]. In this work, we aim at a much more stringent test of $ab\ initio$ calculations by measuring the $2^+_2$ state lifetimes.

In $^{20}$O, the first-excited $2^+_1$ state at 1674 keV decays with a lifetime of 10.4(9) ps [35]. The $2^+_2$ state, of our interest, located at 4070 keV, was found to decay to the $2^+_1$ state with 72(8)% branch [31], in parallel to the direct ground state branch for which contradicting B(E2) information is reported from intermediate-energy Coulomb excitation [36, 37]. In $^{16}$C, the $2^+_2$ state at 1762 keV decays with a lifetime of 11.4(10) ps [33], while for the $2^+_2$ lifetime only the upper limit of 4 ps is known [32, 33]. Theoretical predictions suggest that the lifetimes of these $2^+_2$ states are in the tens-to-hundreds femtoseconds range. This poses an experimental challenge since such neutron-rich systems can only be produced, with sizable cross sections, in: i) relativistic heavy-ion fragmentation, for which the lower limit in lifetime determination is few hundreds femtoseconds, as shown by Morse et al. [38], ii) low-energy transfer and deep-inelastic reactions, where the complex structure of the product velocity distribution, caused by large energy dissipations [39,40], does not allow to use standard Doppler Shift Attenuation Methods [41].

In this work, we have developed a technique which enables us to access tens-to-hundreds femtoseconds life-
The novelty of the method relies on the accurate reconstruction of the complex initial velocity distribution of the reaction product excited to a specific nuclear state, including contributions from direct and dissipative processes. The Doppler-shifted \( \gamma \)-transition line shape is then simulated considering the precisely determined detection angle between the \( \gamma \)-ray and the reconstructed initial product velocity inside the target. It will be shown that the required sensitivity to the lifetimes could only be achieved by the excellent performances of our integral AGATA+PARIS+VAMOS detection system.

In the present study, \( ^{16}\)C and \( ^{20}\)O nuclei were populated in both direct transfer and deep-inelastic processes induced by an \( ^{18}\)O beam at 126 MeV on a \( ^{181}\)Ta target (6.64 mg/cm\(^2\)). The beam energy at the center of the target was \( \sim 116 \) MeV, i.e., \( \sim 50\% \) above the Coulomb barrier, and projectile-like products had velocity \( v/c \sim 10\% \).

The experiment was performed at GANIL with 31 High-Purity Ge detectors of the AGATA array \([43, 44]\), coupled to a scintillator array consisting of two large volume (3.5”\( \times \)8”) \( \text{LaBr}_3 \) detectors plus two clusters of the PARIS setup \([45]\), which produced excellent time reference for the reaction. Reaction products were detected in the VAMOS++ spectrometer \([46, 47]\), placed at the reaction grazing angle of 45° (opening angle \( \pm 6° \)) with respect to the beam direction and aligned with the center of AGATA. Relative to the VAMOS++ axis, AGATA covered the 115°-175° angular range, while the scintillators were placed at 90°. More than \( 10^8 \) events were collected requiring coincidences between projectile-like products detected in VAMOS++ and \( \gamma \) rays in AGATA or PARIS. The VAMOS++ setting was optimized to detect \( ^{20}\)O within a large velocity range, including quasi-elastic and deep-inelastic processes. Other products with charge \( 5 \leq Z \leq 9 \) and mass number \( 11 \leq A \leq 21 \) were also detected.

Identification plots of O and C ions are given in Fig. 1 together with the velocity distributions measured in VAMOS++ for the \( 2^+ \) states in \( ^{20}\)O and \( ^{16}\)C. In the case of \( ^{20}\)O, the velocity distribution shows a pronounced peak, corresponding to the direct population in a quasi-elastic process, while the tail, extending towards lower velocities, is associated with higher kinetic energy loss. The velocity distribution is similar in \( ^{16}\)C, although with a much larger contribution (\( \sim 32\% \)) from dissipative processes.

Portions of \( \gamma \)-ray spectra obtained with AGATA by gating on \( ^{19}\)O, \( ^{20}\)O and \( ^{16}\)C ions, Doppler-corrected considering the product velocity vector measured in VAMOS++, are shown in Fig. 2 panels a), b) and c), respectively. All visible \( \gamma \) rays correspond to known transitions (see level schemes on the right). A closer inspection reveals that some of the peaks are narrow and their energies agree, within uncertainty, with earlier studies. This is the case of transitions from relatively long-lived levels (\( \tau > 1 \) ps), emitted in flight outside the target, as for example the 1375-keV and 2371-keV lines in \( ^{19}\)O, the 1674-keV line in \( ^{20}\)O and the 1762-keV peak in \( ^{16}\)C \([48]\).

In contrast, other lines, depopulating states with lifetimes shorter than 1 ps, exhibit rather large widths and tails. This indicates that the corresponding \( \gamma \) rays were partly emitted during the stopping process of the reaction product inside the target, i.e., at larger velocity than the one measured in VAMOS++. In these cases, the Doppler-broadened line shape can be used to determine the lifetime of the state.

The Monte Carlo simulation of the Doppler-shifted \( \gamma \)-transition line shapes was performed in three steps \([49]\). First, we reconstruct, iteratively, the initial product velocity distribution inside the target, associated with the population of a given state (see Fig. 1). The procedure is based on the VAMOS++ measured velocity-angle distribution (the spectrometer response function is considered \([47]\)), the reaction kinematics calculated for the selected state (including direct population and more dissipative processes), a random probability of reaction occurrence over the target thickness, and the slowing-down and straggling processes inside the target, from Ziegler et al. (1975).
al. [50-51]. Second, we simulate the Doppler-shifted energy measured in AGATA for a transition emitted by the moving product nucleus, with lifetime and transition energy as parameters. Here, the angle between the product velocity at the emission point and the γ energy as parameters. Here, the angle between the product moving product nucleus, with lifetime and transition energy measured in AGATA for a transition emitted by the 9/2+ state in 20O.

We now turn to the lifetime of the 2+ states in 20O and 16C. Figures 3(g)-(i) refer to the 2+ → 2+ decay in 20O. A well-defined minimum is found in the γ2 surface, yielding the values $\tau = 2394.6^{+1.0}_{-1.0}$ keV and $\gamma = 150^{+80}_{-30}$ fs. We note that the γ-ray energy agrees with the most precise value reported in literature, $E_\gamma = 2396(1)$ keV [31], while the present determination of the lifetime is the first obtained thus far. For the $2^+_2 \rightarrow 2^+_1$ decay, considering its 79(5)% branching ratio, here determined, one gets a partial lifetime of 100+102 −40 fs. We stress that the above results rely on the AGATA excellent position resolution of the first γ interaction point, determined with the combined use of Pulse Shape Analysis [54-55] and the Orsay Forward Tracking algorithm [56]. Defining the γ direction from the front segment centers only, as in the case of conventional Ge arrays, gives χ2 minima with much larger uncertainty (dashed lines in the insets of Fig. 3(b)-(g)), making meaningless a comparison with theory.

Figures 3(j)-(k) report the analysis of the 2+ state in 16C, performed on the γ-ray spectrum integrated over the entire angular range, i.e., 120°-180°, due to the limited statistics. As a consequence, the 16C χ2 map, shown in Fig. 3(j), displays a wide valley, resulting in a very limited sensitivity when $E_\gamma < 2216$ keV. For $2^+_2 \rightarrow 2^+_1$ transition energies $E_\gamma > 2216$ keV, the procedure provides a more definite value, which would indicate a lifetime $\gamma < 180$ fs. Considering the most precise energy measurement $E_\gamma = 2217(2)$ keV [33], there is a 78% probability for this scenario.

We performed calculations for 20O by employing chiral NN interactions based on Ref. [87], and 3N interactions fitted on top, considering only few-body systems up to 4He. First, the many-body perturbation theory (MBPT) valence-shell interactions from Ref. [8] were employed with an 16O core. NN and normal-ordered 3N interactions are included up to third order, neglecting residual 3N interactions. Effective operators are used to calculate EM transitions [58-59]. The shell model diagonalizations were performed with the code ANTOINE [60]. The MBPT results reproduce well the $2^+_2 \rightarrow 0^+$ lifetime in 20O ($\tau = 11.7$ ps vs. the experimental $\tau = 10.5(4)$ ps [34]), and this agreement does not depend significantly on the inclusion of 3N interactions. In turn, as shown in Fig. 4 the calculated partial lifetime of the $2^+_1 \rightarrow 2^+_1$ decay, $\tau = 275$ fs (dashed blue line), agrees well with the present measurement only when 3N interactions are considered (B(M1)=0.015 $\mu_N^2$, B(E2)=0.051 e²fm⁴, taking the experimental transition energy). When they are neglected, the $2^+_1 \rightarrow 2^+_1$ partial lifetime is about 60%
The good agreement with the experimental lifetime also suggests a small impact of meson-exchange currents, not included in this calculation.

In $^{10-20}\text{C}$ isotopes, Forssén et al. have performed NCSM calculations with NN+3N interactions \cite{30}. Like in the VS-IMSRG, total energies and transition probabilities are obtained without effective charges or additional parameters. Consistently with the MBPT calculation on $^{20}\text{O}$, Forssén et al. find the decay rates of the $2^{+}$, $3^{+}$, and $4^{+}$ excited states in $^{16}\text{C}$ sensitive to 3N forces, with transition strengths reduced up to a factor 7. For the $2^{+} \rightarrow 1^{+}$ decay, the NCSM finds that the $B(M1)=0.063 \mu_{N}^{2}$ dominates, yielding the partial lifetime $\tau = 81$ fs. Figure \ref{fig:1} shows that the NCSM calculations are consistent with the experimental estimates for transition energy $E_{\gamma} \geq 2216$ keV – this scenario has 78% probability, as discussed above. The absence of a 3980-keV $2^{+} \rightarrow 0^{+}$ decay branch in our data, for which we extract an upper limit of $\leq 8.8\%$ \cite{33} is also consistent with the NCSM NN+3N results.

Summarizing, we have measured, for the first time, the transition strength reduced up to a factor 7. For the $2^{+} \rightarrow 1^{+}$ decay, the NCSM finds that the $B(M1)=0.063 \mu_{N}^{2}$ dominates, yielding the partial lifetime $\tau = 81$ fs. Figure \ref{fig:1} shows that the NCSM calculations are consistent with the experimental estimates for transition energy $E_{\gamma} \geq 2216$ keV – this scenario has 78% probability, as discussed above. The absence of a 3980-keV $2^{+} \rightarrow 0^{+}$ decay branch in our data, for which we extract an upper limit of $\leq 8.8\%$ \cite{33} is also consistent with the NCSM NN+3N results.
times in the tens-to-hundreds femtoseconds range, using low-energy transfer and deep-inelastic reactions. This technique will be essential for similar investigations in exotic neutron-rich nuclei produced with intense ISOL-type beams. Crucial in our work was the high precision 3N interactions needed to accurately describe electromagnetic observables in neutron-rich nuclei. From a broader perspective, the present measurement demonstrates that high-precision γ spectroscopy can benchmark first principles nuclear structure calculations. The work paves the way toward comprehensive tests of ab initio approaches, exploiting electromagnetic transitions in addition to standard comparisons based mostly on nuclear energies.

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