FORMATION OF A SYSTEM OF MULTICRITERIA INDICATORS FOR THE ASSESSMENT OF OFFICE LEASING OPTIONS

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ABSTRACT. With the growing scope of business and the internationalization of companies, office leasing is becoming an increasingly relevant issue. It has become an integral part of business and affects the results of commercial activities. The methods for the assessment of office leasing options that are available at the moment are imperfect, as they lack complexity and they are not related to the objective of the lease – the improvement of business results, imperfect methods for a quantitative assessment of the lease options, etc. The adequacy of the assessment of lease options largely depends on the system of indicators that is used. The system is formed on the basis of a list of indicators composed from different sources. For the system of indicators to fully reflect the analyzed phenomenon and to be suitable for a quantitative assessment, there have to be not too many or too few indicators in the system. This means that the indicators that are insignificant have to be eliminated from the list. The most precise way to do that is to apply methods of mathematical statistics. The research is based on the analysis of scientific literature and the methods of mathematical statistics.

KEYWORDS: Lease of offices; Indicators of lease options; Formation of a system of indicators; Multicriteria assessment; Expert assessment

1. INTRODUCTION

The formation of the system of indicators has a special role in multicriteria assessments. This is because the adequacy of the reflection of the analyzed phenomenon depends on this system. Despite its importance, this phase of the multicriteria assessment is not given enough attention. In some cases, the system of indicators is simply identified with a pre-formed list of indicators; and in other, where the question of eliminating or keeping certain indicators in the system is analyzed, it is done without a sufficiently methodical basis.

The list of indicators reflecting the analyzed phenomenon (AP) usually covers a potentially high number of indicators (Podvezko 2008; Zavadskas, Turskis 2011). It is considered that the more extensive the list, the better the AP is reflected. Secondly, the indicators on the list are not equally important to the analyzed phenomenon – some of them are insignificant. Such indicators should not be included in the system, which is the basis for the AP assessment, as they will not increase the accuracy of the assessment, but will significantly encumber the calculations. Thus, insignificant indicators should be eliminated. Generally, the following statements are followed when forming a system for a multicriteria assessment based on a list of indicators (Ginevičius, Podvezko 2005): first of all, the more indicators that are included into the system, the more accurate the reflection of the analyzed phenomenon will be; and conversely, the fewer indicators that are included into the system, the higher the risk is that significant AP indicators will remain unanalyzed and the assessment of the state of the AP may prove to be inadequate. Secondly, the more indicators that are included, the more indicators there will be that are difficult to formalize, and besides the system becoming more complex, it will be more difficult to accurately determine the significance of the indicators. As a
result, the cost of the calculations will increase, and their accuracy will decrease. This leads to the conclusion that the number of indicators included into the system cannot be too low or too high.

An analysis of the sources of literature shows that there are two possible methods of forming a system of indicators. The first one is limited to those indicators mentioned most often in the sources of literature and other sources (Brauers et al. 2014; Ginevičius, Podvezko 2013; Nugaras, Ginevičius 2015). It is the most basic, but also a less accurate method. The second method uses the more complex but significantly more accurate methods of mathematical statistics (Ginevičius, Podvezko 2005; Ginevičius et al. 2013; Kondyli 2010; Boggia, Cortina 2010; Buracas et al. 2012; Mardani et al. 2015a, 2015b; Kim et al. 2015; Bausys, Zavadskas 2015; Keshavarz Ghorabaee et al. 2015; Hashemkhani Zolfani et al. 2015; Liu et al. 2016; Kou et al. 2016).

The aim of the article is to form a system of indicators for the leasing of commercial real estate objects (offices) from a list compiled by applying the methods of mathematical statistics. The research is based on an analysis of the scientific literature and on the methods of mathematical statistics.

2. FORMATION OF THE SYSTEM OF INDICATORS BY APPLYING THE METHODS OF MATHEMATICAL STATISTICS

An analysis of the sources of literature allows us to distinguish certain typical methods of the formation of a list of indicators for the analyzed phenomenon. In the simplest cases, indicators are included in the list without any justification. It would seem that the author bases their inclusion solely on his/her opinion; therefore, this is the most subjective way of forming a list (Azbainis, Rudzkiene 2011). The most common cases are when the list is based solely on the sources of literature (Russell 2002; Turskis et al. 2009; Ball et al. 2012; Pagourtzi et al. 2003; Golusin, Munitlak Ivanovic 2009). The third method, which is rather rare, is when the list of indicators is based on an expert assessment. Another rare method is when a list is formed on the basis of the sources of literature and other sources, as well as expert assessment (French, Wiseman 2003; Nase et al. 2013; Jokiene, Zvirblis 2014).

The latter is the best method, as it evaluates international experience, and, thanks to the expert assessment also takes into consideration the specific aspects of the country where the research is taking place.

This article is based on this method of the formation of the list of indicators for the analyzed phenomenon. In any event, an initial table has been drawn up for the list of AP indicators highlighting the indicators most often mentioned or suggested in the sources of literature (Čeh et al. 2012; Nase et al. 2013; Au-Yong et al. 2014) as well as by the experts (Table 1).

Based on the sources of literature and other sources, as well as the opinions of 21 experts, Table 1 has been drawn up. 59 indicators were defined. All of them could be divided into three blocks according to their similarities: economic indicators – 14; indicators describing the atmosphere and potential of the premises – 27; and indicators describing the infrastructure of the environment and location – 18 (Fig. 1).

| No. | Name of source | Indicators |
|-----|----------------|------------|
| 1   |                | +          |
| 2   |                | +          |
| 3   |                | +          |
| ... |                | +          |
| 1   |                | +          |
| ... |                | +          |
| ... |                | +          |
| M   |                | +          |

| Total | \( \sum_1 \) | \( \sum_2 \) | \( \sum_3 \) | ... | \( \sum_i \) | ... | \( \sum_n \) |
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| ECONOMIC INDICATORS | ENVIRONMENT | PREMISES |
|---------------------|-------------|----------|
| INFRASTRUCTURE      | LOCATION    | TECHNICAL LEVEL OF EQUIPMENT |
| INTERNAL FACTORS    | POSIBILITIES |

### ECONOMIC INDICATORS
1. Rent
2. Lease period
3. Existence of requirements with respect to work time
4. Additional infrastructure fees (parking, waste elimination, building administration, heating substation maintenance, etc.)
5. Real estate fee
6. Fees for common premises
7. Existence and amount of surety
8. Method of calculation of rent
9. Additional conditions
10. Price of heating and method of calculation
11. Price of illumination and method of calculation
12. Fees for joint advertising
13. Property management fee
14. Procedure of termination of the agreement

### ENVIRONMENT
1. Appearance of adjacent buildings and environment
2. View through the windows of the office
3. Size of parking lot (number of spaces)
4. Prestige of location and demand for location
5. Distinction and prestige of organizations located in adjacent buildings
6. Noisiness of the environment of the building
7. Visibility of the building
8. Distance to parking lot
9. Distance to a public transport stop
10. Distance to the parking lot
11. Pollution of the district
12. Distance to banks and other establishments
13. Distance to city center
14. Safety of neighbourhood
15. Distance to restaurants, shopping, sport centers, etc.
16. Traffic jams on the way to the office
17. Activity of the business environment
18. Distance from residential neighbourhoods
19. Year of construction of the building
20. Elevator
21. Aesthetic appearance of the building (exterior, interior)
22. Fire safety system
23. External and internal architectural solutions of the building
24. Degree of equipment of the building
25. Level of engineering constructions
26. Functionality of premises
27. Quality of illumination, heating and ventilation systems of premises
28. Quality of interior finish
29. Amount of natural light in the premises
30. Materials used for construction of the building
31. Is the building certified

### PREMISES
1. Building lessees
2. Lessor's view of the lessee
3. Procedure of administration of the building
4. Distinction and prestige of organizations located in the building
5. Management of maintenance of the building
6. Form of ownership of the building
7. Ability to place advertisements
8. IT communications
9. Possibility to choose the floor of the building
10. Satisfaction of the needs of the lessee with respect to premises
11. Possibility to change parameters of premises
12. Security of the building
13. Easy access to the premises
14. Percentage of occupation of the building

Fig. 1. System of lease indicators for commercial real estate objects (offices)
Such a grouping helps the experts to adequately rank the indicators according to their importance. The elimination of insignificant indicators is based on a histogram obtained by placing the indicators at respective intervals, according to their rate of mentioning, i.e. their rank. Its configuration is thus also the theoretical probability distribution of a random value $X$, whose description largely depends on the manner of grouping the ranks of the indicators. In order to draw up a histogram, first of all we need to rank the indicators of all three blocks, according to their importance. Rank 1 is given to the most important indicator and rank $n$ – to the least important indicator (where $n$ is the number of indicators in a block). In our case, the value $X$ shows the number of times the same rank of the indicator was given in the questionnaires by the experts. Interval $[X_{i-1}, X_i]$ shows that indicators $n_i$ were mentioned in all questionnaires by the experts from $i-1$ to $i$ times, e.g. $[0,6]$, $n_i = 4$. This shows that 4 indicators were mentioned in all questionnaires from 0 to 5 times (6 is not covered by the interval). The results of the ranking of all three blocks of lease indicators – economic, environment and premises – are presented in Tables 2–4.

### Table 2. Results of the ranking of importance of the economic lease indicators

| No. | Name of indicator                                      | Experts | Total |
|-----|--------------------------------------------------------|---------|-------|
| 1.  | Rent                                                   | 1 1 1 2 1 1 1 1 2 2 2 2 2 1 1 1 1 1 1 1 27 |
| 2.  | Lease period                                           | 14 12 13 14 14 12 13 12 13 14 14 14 11 11 14 12 13 13 273 |
| 3.  | Existence of requirements with respect to work time    | 13 11 14 10 14 10 13 13 10 8 8 9 12 10 10 14 11 14 14 12 240 |
| 4.  | Additional infrastructure fees (parking, waste elimination, building administration, heating substation maintenance, etc.) | 3 2 2 1 5 2 3 2 3 1 1 1 1 1 9 2 2 2 2 2 3 51 |
| 5.  | Real estate fee                                        | 7 6 6 7 3 5 6 3 5 5 4 4 3 8 4 7 6 5 4 8 8 114 |
| 6.  | Fees for common premises                              | 12 9 9 11 12 7 12 9 11 14 12 12 10 10 9 9 12 13 11 9 7 220 |
| 7.  | Method of calculation of rent                          | 6 8 11 6 8 4 10 10 8 7 11 11 7 11 8 8 10 9 10 5 6 174 |
| 8.  | Existence and amount of surety                         | 5 10 4 8 6 11 11 5 6 11 3 5 4 4 6 3 4 7 7 6 4 130 |
| 9.  | Additional conditions                                  | 9 14 10 12 7 9 8 6 12 13 10 10 13 13 11 12 13 12 13 11 5 222 |
| 10. | Price of heating and method of calculation             | 10 5 5 13 4 13 7 7 7 4 7 7 6 7 12 14 8 6 9 12 11 174 |
| 11. | Price of illumination and method of calculation        | 8 7 12 5 9 3 2 8 9 6 9 9 11 5 3 4 9 3 6 7 9 144 |
| 12. | Fees for joint advertising                            | 2 3 7 4 2 6 5 4 1 3 5 3 5 2 5 5 3 4 3 3 2 77 |
| 13. | Property management fee                                | 4 13 8 9 10 12 9 14 14 9 14 14 12 6 13 13 7 8 8 10 14 221 |
| 14. | Procedure of termination of the agreement              | 11 4 3 3 11 8 4 11 4 8 6 6 8 3 7 6 5 10 5 4 10 137 |

### Table 3. Results of ranking of importance of premises lease indicators

| No. | Name of indicator                                      | Experts | Total |
|-----|--------------------------------------------------------|---------|-------|
| 1.  | Year of construction of the building                   | 21 26 17 16 16 11 25 27 12 27 24 11 4 4 18 16 12 25 20 22 19 373 |
| 2.  | Elevator                                               | 23 14 22 13 11 10 17 13 20 10 20 20 21 27 7 18 13 6 23 21 16 339 |
| 3.  | Aesthetic appearance of the building (exterior, interior) | 4 6 5 12 12 15 16 11 17 11 17 25 1 1 3 5 15 11 14 1 9 201 |

(Continued)
| No. | Name of indicator                                                                 | Experts | Total |
|-----|-----------------------------------------------------------------------------------|---------|-------|
| 4.  | Fire safety system                                                                 | 17 23 9 24 20 24 22 10 21 9 18 5 11 11 17 19 10 14 13 20 10 327 |
| 5.  | External and internal solutions of the building                                    | 13 5 21 5 8 16 14 22 3 25 19 18 17 17 15 21 16 13 12 27 13 320 |
| 6.  | Degree of equipment of the building                                               | 1 16 10 17 1 3 15 26 6 19 3 6 24 5 5 6 3 7 6 19 8 205 |
| 7.  | Level of engineering communications                                              | 16 2 14 7 7 19 13 9 11 15 16 17 9 9 14 23 4 10 5 17 7 244 |
| 8.  | Functionality of premises                                                          | 5 7 2 3 3 4 17 6 8 2 6 2 16 8 8 22 8 2 4 4 14 5 153 |
| 9.  | Quality of illumination, heating and ventilation of premises                      | 3 8 4 8 6 20 2 7 14 7 9 8 14 14 13 24 20 8 18 25 4 236 |
| 10. | Quality of interior finish                                                          | 12 18 27 10 3 9 10 5 15 16 4 13 6 6 12 10 18 19 19 11 3 246 |
| 11. | Amount of natural light in the premises                                           | 19 9 13 19 26 25 7 3 10 2 14 10 20 20 10 13 19 3 24 6 24 296 |
| 12. | Materials used for the construction of the building                               | 20 19 12 22 19 21 24 20 23 26 26 7 25 25 27 21 20 17 26 22 449 |
| 13. | Is the building certified                                                           | 26 25 24 25 24 7 8 23 27 18 27 3 19 19 26 12 9 27 25 7 27 408 |
| 14. | Lessees of the building                                                            | 10 21 20 27 27 13 20 21 16 24 22 27 22 22 16 2 27 18 13 3 13 391 |
| 15. | Lessor's view of the lessee                                                         | 7 11 18 15 5 2 3 15 17 5 5 21 23 23 11 17 26 16 1 3 14 258 |
| 16. | Procedure of administration of the building                                       | 6 12 19 11 5 14 27 14 18 20 6 4 10 10 23 3 22 2 12 15 17 270 |
| 17. | Distinction and prestige of organizations located in the building                 | 24 15 8 20 22 4 4 18 8 23 7 26 16 16 24 20 23 21 15 18 21 353 |
| 18. | Management of maintenance of the building                                         | 8 27 15 18 13 18 5 19 22 22 8 6 24 24 21 7 17 15 16 16 6 322 |
| 19. | Ownership type of the building                                                     | 27 27 25 21 23 26 26 25 25 8 12 2 27 27 25 26 25 26 27 9 25 464 |
| 20. | Ability to place advertisements                                                    | 22 4 16 14 17 27 21 17 19 13 23 23 23 15 15 19 14 11 17 22 4 15 348 |
| 21. | IT communications                                                                  | 11 3 7 9 10 12 19 16 13 4 21 22 12 12 4 15 5 2 21 10 12 240 |
| 22. | Possibility to choose the floor of the building                                    | 25 13 6 2 21 23 18 12 5 3 10 19 2 2 6 4 6 22 11 5 11 226 |
| 23. | Satisfaction of the needs of the lessee with respect to the premises               | 2 1 1 4 2 1 1 6 1 1 1 15 13 13 1 9 1 1 7 12 1 94 |
| 24. | Possibility to change parameters of premises                                      | 18 20 26 23 18 8 23 4 21 15 10 14 18 18 8 11 8 24 8 24 23 356 |
| 25. | Security of the building                                                           | 15 17 11 1 15 22 12 6 1 14 25 1 7 7 9 25 14 10 9 23 8 255 |
| 26. | Easy access to the leased premises                                                 | 14 10 3 6 14 5 9 2 4 12 11 12 3 3 2 22 7 5 9 2 2 157 |
| 27. | Percentage of occupation of the building                                          | 9 24 23 26 25 6 11 24 26 17 13 9 26 26 20 1 24 23 26 8 26 393 |
Table 4. Results of ranking of importance of environment indicators

| No. | Name of indicator                                      | Experts | Total |
|-----|--------------------------------------------------------|---------|-------|
| 1.  | Pollution of the district                              | 17 9 7 7 16 17 9 6 4 5 12 1 | 221 |
| 2.  | Appearance of adjacent buildings and environment        | 6 8 9 5 10 13 10 14 13 3 11 3 9 4 1 9 15 7 13 2 13 18 5 18 14 1 18 4 221 |
| 3.  | Distance to banks and other establishments              | 18 13 10 12 4 2 13 7 16 2 10 15 8 8 3 10 6 10 14 6 11 200 |
| 4.  | Size of parking lot (number of spaces)                 | 12 17 11 15 18 15 17 18 12 12 13 14 10 7 1 11 9 18 15 15 14 276 |
| 5.  | Distance to residential neighbourhoods                 | 13 18 3 17 17 18 12 17 18 7 18 4 13 6 18 15 17 16 17 14 12 292 |
| 6.  | Distance to city centre                                | 1 16 1 11 9 6 16 16 7 2 9 10 11 3 12 7 5 5 16 5 8 178 |
| 7.  | Security of the neighbourhood                          | 3 3 8 9 11 8 15 4 11 6 17 2 17 10 2 12 10 12 2 13 15 192 |
| 8.  | View through the windows of the office                | 8 6 10 6 15 14 14 8 9 9 14 7 12 11 5 13 14 11 18 12 7 225 |
| 9.  | Distance to restaurants, shopping, sport centres, etc. | 7 12 2 8 6 3 11 3 17 7 15 8 16 13 3 8 3 15 12 11 3 185 |
| 10. | Traffic jams on the way to the office                  | 9 14 6 3 2 4 3 5 5 5 16 9 14 12 5 16 16 6 7 16 9 184 |
| 11. | Size of parking lot                                    | 2 5 4 10 3 1 1 2 3 1 4 13 4 1 1 1 8 4 3 10 2 84 |
| 12. | Prestige of location and demand for location           | 4 1 12 8 5 7 2 1 1 1 3 18 5 2 1 2 4 2 8 17 5 110 |
| 13. | Distinction and prestige of organizations located in adjacent buildings | 10 7 5 11 12 9 6 9 6 4 2 17 2 5 8 3 7 8 9 4 6 151 |
| 14. | Noisiness of environment of the building               | 16 4 15 17 13 10 7 10 10 8 8 5 15 17 9 14 13 13 4 9 17 236 |
| 15. | Visibility of the building                            | 11 15 13 10 14 11 8 15 15 1 5 16 6 9 1 4 2 9 5 1 16 188 |
| 16. | Activity of the business environment                  | 5 2 17 2 1 5 18 13 8 5 1 12 1 18 5 3 5 1 1 6 2 1 128 |
| 17. | Distance to parking lot                                | 14 10 16 5 8 12 4 11 2 2 6 11 3 15 2 6 11 3 10 3 10 165 |
| 18. | Distance to a public transport stop                    | 15 11 14 6 7 16 5 12 14 3 7 5 7 14 15 18 12 17 11 8 18 236 |

After ranking the importance of the blocks of indicators, the compatibility with the expert opinions was verified using the criterion $\chi^2$. The results of these calculations are presented in Table 5.

Table 5. Results of the verification of the compatibility with expert assessments of the importance of the office lease indicators

| No. | Name of block of indicators | Value of Pearson criterion $\chi^2$ | Calculated | Critical |
|-----|-----------------------------|------------------------------------|------------|----------|
| 1.  | Economic                    | 192.90                             | 23.68      |
| 2.  | Premises                    | 86.13                              | 31.45      |
| 3.  | Environment                 | 79.54                              | 27.59      |

It can be seen from Table 5 that in all three cases, the calculated value of criterion $\chi^2$ is higher than the critical value, which means that the opinions of the experts are compatible.

After verifying the opinions of the experts with the ranks of all three blocks, we can determine the intervals of change of the random value $X$, as well as the number of indicators that are covered by such intervals. We will use the lowest and highest sum of the ranks in every block for this purpose (Table 6).

Table 6. Lowest and highest sums of the ranks for the commercial real estate (office) lease indicators

| No. | Name of block of indicators | Lowest and highest sums of ranks of indicators |
|-----|-----------------------------|-----------------------------------------------|
| 1.  | Economic                    | 27 273                                        |
| 2.  | Premises                    | 90 432                                        |
| 3.  | Environment                 | 84 292                                        |
Now we can determine the size of the intervals based on the formula:

\[ h_i = \frac{S_{\text{max}} - S_{\text{min}}}{5}, \]

where: \( h_i \) – interval of the block of indicators \( i \); \( S_{\text{max}} \) – highest sum of the ranks of the block of indicators \( i \) for all indicators of \( i \); \( S_{\text{min}} \) – lowest sum of the ranks of the block of indicators \( i \) for all values of this block.

The rank change interval \( S_{\text{max}} - S_{\text{min}} \) is divided into five parts, so that after finally combining all three blocks of indicators every interval will contain not less than 5 indicators.

Now the blocks of indicators can be grouped according to their intervals (Tables 7–9).

The results of the grouping of the indicators for all three blocks are presented in Table 10.

The elimination of insignificant indicators from the list is based on a histogram obtained by placing the values of the indicators at certain intervals and determining the frequency that those indicators were mentioned. Its configuration is thus also the theoretical probability distribution of the random value \( X \), and its description largely depends on the manner of grouping of the results of the ranking of the indicators. In order to draw up a histogram, first of all we need to rank the indicators of all three blocks according to their importance, giving rank 1 to the most important indicator and rank \( n \) to the least important indicator (where \( n \) is the number of indicators in a block). The value \( X \) shows the number of times that the indicator was mentioned in the expert questionnaires (\( 0 \leq X \leq Z \), where \( Z \) is the number of experts).

Based on Tables 7–10, a histogram of the importance of the economic, premises and environment indicators can be drawn up (Figs. 2–4).

### Table 7. Results of the grouping of the economic lease indicators

| Intervals    | [27;75] | [75;125] | [125;175] | [175;225] | [225;275] |
|--------------|---------|---------|---------|---------|---------|
| Frequency    | 2       | 3       | 4       | 3       | 2       |

### Table 8. Results of the grouping of the premises indicators

| Intervals    | [83;157] | [157;231] | [231;305] | [305;379] | [379;453] |
|--------------|---------|---------|---------|---------|---------|
| Frequency    | 3       | 6       | 8       | 7       | 3       |

### Table 9. Results of the grouping of the environment indicators

| Intervals    | [82;124] | [124;166] | [166;208] | [208;250] | [250;292] |
|--------------|---------|---------|---------|---------|---------|
| Frequency    | 2       | 3       | 7       | 3       | 2       |

### Table 10. Results of the grouping of the lease indicators according to their importance

| Name of block of indicators | Interval number | Total |
|-----------------------------|-----------------|-------|
|                             | Interval limits | Frequency |
| Economic                    | [27;75]         | 2      |
|                             | [75;125]        | 3      |
|                             | [125;175]       | 4      |
|                             | [175;225]       | 3      |
|                             | [225;275]       | 2      |
| Total                       |                 | 14     |
| Premises                    | [83;157]        | 3      |
|                             | [157;231]       | 6      |
|                             | [231;305]       | 8      |
|                             | [305;379]       | 7      |
|                             | [379;453]       | 3      |
| Total                       |                 | 27     |
| Environment                 | [82;124]        | 2      |
|                             | [124;166]       | 3      |
|                             | [166;208]       | 7      |
|                             | [208;250]       | 3      |
|                             | [250;292]       | 2      |
| Total                       |                 | 17     |
Now we can draw up a collective histogram of the importance of the lease indicators. For this purpose, we need to start by determining the collective results of the ranking of the importance of the indicators, and then to determine the size of the intervals and the total number of indicators covered by the intervals based on the formula (1) (Table 11).

Based on Table 11, we can draw up a collective histogram of the importance of the lease indicators (Fig. 5).

As can be seen from Table 11, every interval contains at least 5 indicators. We can also see that a hypothesis that the random value \( X \) is distributed according to a normal distribution can be presented. Based on this table, we can calculate the parameters of the distribution – mean \( \bar{X} \) and average square deviation \( S \). From this, we determined that \( \bar{X} = 619.6 \) and \( S = 196 \). Based on the table of the normal distribution, we calculated theoretical probability \( P_i \) that the random value \( X \) belongs to a certain interval \( (X_{i-1}, X_i) \), and the theoretical frequencies \( n_i^* = nP_i \). The results of the calculations are presented in Table 12.

| Intervals       | Frequency |
|-----------------|-----------|
| [202;2368)      | 7         |
| [2368;2518)     | 12        |
| [2518;2937)     | 19        |
| [2937;3500)     | 13        |
| [3500;4147)     | 7         |
| Total           | 58        |

Table 11. Collective results of the ranking of the importance of the lease indicators

Theoretical frequencies of all lease indicators are presented in Figure 5. Now we need to verify whether the hypothesis that the importance of the commercial real estate object (office) lease is distributed according to a normal distribution is correct. For this purpose, we needed to calculate the actual and critical values of the criterion \( \chi^2 \) with the degrees of freedom \( \gamma = k - 3 - 1 = 2 \) and the level of significance \( \alpha = 0.05 \). The results are \( \chi^2 = 5.99 \) and \( \chi^2_{kr} = 0.574 \).

The calculated value \( \chi^2 \) is higher than the critical value; therefore, the hypothesis that the value \( X \) is distributed according to a normal distribution with the mean of \( X = 619.6 \) and the average square deviation \( S = 196 \) is accepted. This shows which indicators from the last intervals may be eliminated.

For this purpose, we need to determine the percentage of unnecessary indicators to be eliminated. If we assume that this number is 10% (i.e. the level of significance \( \alpha = 0.1 \)), then by applying the inequality \( P(X_{kr} \leq X \leq +\infty) = 0.1 \) from the normal distribution table, we can determine that \( X_{kr} = 870.48 \), i.e. the indicators whose sum of their ranks is higher than 870.48 should be eliminated from the general list of indicators. These are the indicators from the last interval (Fig. 5). They include 2 indicators from the economic block, 3 indicators from the premises block and 2 indicators from the environment block.

The final list of indicators to be included in the system for commercial real estate object (office) leasing is as follows (Table 13).
Table 13. System of indicators for commercial real estate object (office) leasing

| No. | Blocks of lease indicators | Economic | Environment | Premises |
|-----|----------------------------|----------|-------------|---------|
| 1   | Rent                       | Appearance of adjacent buildings and environment | Year of construction of the building |
| 2   | Period of lease            | View through the windows of the office | Elevator |
| 3   | Existence of requirements with respect to work time | Size of parking lot (number of spaces) | Aesthetic appearance of the building (exterior, interior) |
| 4   | Additional infrastructure fees (parking, waste elimination, building administration, heating substation maintenance, etc.) | Prestige of location and demand for location | Fire safety system |
| 5   | Real estate fee            | Distinction and prestige of organizations located in adjacent buildings | External and internal architectural solutions of the building |
| 6   | Fees for common premises   | Noisiness of the environment of the building | Degree of equipment of the building |
| 7   | Existence and amount of surety | Visibility of the building | Level of engineering communications |
| 8   | Method of calculation of rent | Distance to parking lot | Functionality of premises |
| 9   | Additional conditions      | Distance to a public transport stop | Quality of illumination, heating and ventilation systems of the premises |
| 10  | Price of heating and method of calculation | Pollution of the district | Quality of interior finish |
| 11  | Price of illumination and method of calculation | Distance to banks and other state establishments | Amount of natural light in the premises |
| 12  |                            | Distance to city centre | Lessees of the building |
| 13  |                            | Safety of neighbourhood | Lessor’s view of the lessee |
| 14  |                            | Distance to restaurants, shopping, sports centres, etc. | Procedure of administration of the building |
| 15  |                            | Traffic jams on the way to the office | Distinction and prestige of organizations located in adjacent buildings |
| 16  |                            | Efficiency of business environment | Procedure of maintenance of the building |
| 17  |                            |                                | Possibility to place advertisements |
| 18  |                            |                                | IT communications |
| 19  |                            |                                | Possibility to choose the floor of the building |
| 20  |                            |                                | Satisfaction of the needs of the lessee with respect to the premises |
| 21  |                            |                                | Possibility to change parameters of premises |
| 22  |                            |                                | Security of the building |
| 23  |                            |                                | Easy access to the leased premises |
| 24  |                            |                                | Percentage of occupation of the building |

Table 13 shows the blocks of 11 economic lease indicators, 16 environment indicators and 24 premises indicators.

This system of indicators needs to be adapted for a multicriteria assessment. This necessity arises due to the fact that we need to know not only the values of the indicators, but also their weights. This is determined by the experts. The accuracy of an expert assessment largely depends on the number of assessed indicators. Where there are not many indicators, the experts can determine their weights quite accurately. However, when their number increases, it becomes more difficult to determine the interrelation of the weights of the indicators with respect to the analyzed phenomenon. This increases the incompatibility of the expert opinions. We can see without proof that an expert can assess the weights of 10–12 indicators...
rather accurately (Ginevičius 2006). The system of indicators presented in Table 12 does not satisfy such conditions; thus, it should be transposed in a manner so that the number of assessed indicators does not exceed the desired number (Ginevičius 2007a, 2007b, 2009).

3. CONCLUSIONS

The adequacy of a multicriteria assessment largely depends on the system of indicators that reflects the analyzed phenomenon. It is formed on the basis of a list of indicators. The system of indicators should contain not too many and not too few indicators. Otherwise, the accuracy of the multicriteria assessment will decrease.

Based on the literature and other sources, a list of 59 indicators for commercial real estate object (office) leasing was compiled. In order to form an accurate system of indicators for leasing, the insignificant indicators had to be eliminated. This was done by applying the methods of mathematical statistics.

The formation of the system of lease indicators was based on the table specifying the names of the indicators, as well as on the frequency that each indicator was mentioned. The elimination of indicators from the list was then done in the following order: the value $X$ was chosen as being similar to the distribution of the frequencies in the table; the interval of change of this value was determined; a histogram of the value $X$ was drawn up; depending on the form of the histogram a theoretical probability distribution was chosen; the parameters of the chosen probability distribution were then calculated (with mean and average square deviations); based on these parameters, the function of the probability distribution $F(x)$ or the density $f(x)$ was determined; the calculation of the theoretical probability $P_i$ that the random value $X$ belongs to any interval $(X_{i-1}, X_i)$ was performed: i.e. the calculation of the respective theoretical frequencies; the statistical hypothesis that the random value $X$ was distributed according to the respective theoretical distribution was verified; and depending on the chosen degree of significance we determined the indicators that needed to be eliminated, as they were insignificant. It was determined that 2 indicators from the economic block, 3 indicators from the premises block and 2 indicators from the environment block could be eliminated from the general list of lease indicators as insignificant.

The theoretical benefit of this article is the suggestion of an adequate method for the formation of the system of indicators for commercial real estate object (office) leasing that is intended to solve the problem of office leasing. The method allows businessmen to more accurately assess the office leasing options which are the most suitable.

Even though the current study has presented several advantages, there are some limitations as well. The indicators need to be determined by means of an expert evaluation, which introduces a certain element of subjectivity.

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