Long-range corrected hybrid meta-generalized-gradient approximations with dispersion corrections

You-Sheng Lin,1 Chen-Wei Tsai,1 Guan-De Li,1 and Jeng-Da Chai1,2,

1Department of Physics, National Taiwan University, Taipei 10617, Taiwan
2Center for Theoretical Sciences and Center for Quantum Science and Engineering,
National Taiwan University, Taipei 10617, Taiwan
(Dated: December 21, 2013)

We propose a long-range corrected hybrid meta-GGA functional, based on a global hybrid meta-GGA functional, M05 [Y. Zhao, N. E. Schultz, and D. G. Truhlar, J. Chem. Phys. 123, 161103 (2005)], and empirical atom-atom dispersion corrections. Our resulting functional, $\omega$M05-D, is shown to be accurate for a very wide range of applications, such as thermochemistry, kinetics, noncovalent interactions, equilibrium geometries, frontier orbital energies, fundamental gaps, and excitation energies. In addition, we present three new databases, IP131 (131 ionization potentials), EA115 (115 electron affinities), and FG115 (115 fundamental gaps), consisting of experimental molecular geometries and accurate reference values, which will be useful in the assessment of the accuracy of density functional approximations.

* Author to whom correspondence should be addressed. Electronic mail: jdchai@phys.ntu.edu.tw.
I. INTRODUCTION

Because of its satisfactory accuracy and modest cost in many applications, Kohn-Sham density functional theory (KS-DFT) \cite{1,2} has become one of the most popular electronic structure methods for large ground-state systems \cite{3,4,5,6}. Its extension for treating excited-state systems, time-dependent density functional theory (TDDFT) \cite{7,8}, has also been widely used.

The crucial ingredient of KS-DFT, the exact exchange-correlation (XC) energy functional $E_{xc}[\rho]$, however, remains unknown and needs to be approximated. Functionals based on the local density approximation (LDA), modeling the XC energy density locally with that of a uniform electron gas (UEG), have been quite successful for nearly-free electron systems \cite{3,4}, though still insufficiently accurate for most quantum chemical applications. Functionals based on the generalized gradient approximations (GGAs), additionally incorporating the gradient of local density into the LDA, have achieved reasonable accuracy in many applications. As an extension of the GGA (for rather restricted set of density variables), meta-GGA (MGGA) offers itself quite naturally. Functionals depending directly on the Laplacian of the density have not been pursued intensively, because of the difficulty of numerical evaluation. MGGAs, which adopt the kinetic energy density as a substitute for the Laplacian, have shown evidences of superiority over GGAs. \cite{9,11}

However, the LDA, GGAs and MGGAs (commonly denoted as DFAs for density functional approximations) are based on the localized model XC holes, while the exact XC hole should be fully nonlocal. Currently, perhaps the most successful approaches to taking into account the nonlocality of XC hole are provided by hybrid DFT methods, incorporating a fraction of the exact Hartree-Fock (HF) exchange into the DFAs. Hybrid density functionals have achieved remarkable accuracy and have expanded the usefulness of DFT for many applications. Noticeably, global hybrid MGGA functionals \cite{12,20}, where the XC energy density depends on the local density, the gradient of local density, a fraction of exact exchange, as well as the exact KS kinetic energy density (a function of the occupied KS orbitals) \cite{21,24}, have been shown to potentially perform better than global hybrid GGA functionals \cite{15,20,25,26}, due to the additional ingredient of kinetic energy density in global hybrid MGGA functionals.

In global hybrid functionals, a small fraction of the exact HF exchange is added to a semilocal density functional. In certain situations, especially in the asymptotic regions of molecular systems, a large fraction (even 100\%) of HF exchange is needed. Aiming to remedy this, long-range corrected (LC) hybrid DFT schemes have been actively developed \cite{27,37}. LC hybrids retain the full HF exchange only for the long-range electron-electron interactions, and thereby resolve a significant part of the self-interaction problems associated with global hybrid functionals.

On the other hand, the development of accurate short-range (SR) exchange density functionals $E_{xc}^{SR}[\rho]$, plays an important role in the progress of LC-DFT. In the first LC scheme, an ansatz for the conversion of any $E_{xc}$ to $E_{xc}^{SR}$ was proposed by Iikura et al. \cite{27}, and has become widely used. However, their resulting LC hybrid GGA functionals
do not outperform the corresponding global hybrid GGA functionals for thermochemistry. In 2006, Vydrov et al. proposed a different LC scheme [31], based on integrating a GGA model exchange hole. Their resulting LC-ω-PBE functional has shown improved performance for thermochemistry and barrier heights, and is comparable to global hybrid GGA functionals such as B3LYP [38, 39]. However, further improvements following this direction require the development of more accurate model exchange holes, which is a quite challenging task.

Another approach to more accurate LC hybrid functionals was proposed by Chai and Head-Gordon [35]. First, augmenting the SR local spin density exchange energy density by a flexible enhancement factor (of the Becke’s 1997 form [40]) and fully reoptimizing the LC functional on a diverse training set, yields the ωB97 functional. Second, including an adjustable fraction of SR HF exchange in the ωB97 functional with the similar reoptimization procedure, leads to the ωB97X functional. ωB97 and ωB97X have been shown to be accurate across a diverse set of test data, containing thermochemistry, kinetics, and noncovalent interactions [35].

However, problems associated with the lack of nonlocality of the DFA correlation hole, such as the lack of dispersion interactions (the missing of van der Waals forces), are not resolved by the LC hybrid schemes. The correlation functionals in typical LC hybrids are treated semilocal, which cannot capture the long-range (LR) correlation effects [41, 42]. To remedy this, the DFT-D scheme was applied [43] to extend the ωB97X functional with damped atom-atom dispersion corrections, denoted as ωB97X-D. Consequently, ωB97X-D can obtain dispersive effects with essentially zero additional computational cost relative to ωB97X. As an alternative approach, ωB97X has also been combined with the double-hybrid methods [44–48], which mix both the HF exchange and nonlocal orbital correlation energy from the second-order perturbation energy expression in wave function theory. The resulting ωB97X-2 functional [37] has yielded very high accuracy for thermochemistry, kinetics, and noncovalent interactions, though its fifth-order scaling with respect to system size may limit its applicability to larger systems.

As the ωB97 series are LC hybrid GGAs, it seems a natural step to develop LC hybrid MGGAs and to assess their performance. In this work, we propose a new LC hybrid MGGA-D functional, denoted as ωM05-D, which is shown to be accurate for a wide range of applications, when compared with the two closely related functionals: a global hybrid MGGA functional (M05-2X) [19] and a LC hybrid GGA-D functional (ωB97X-D) [36]. The rest of this paper is organized as follows. In Sec. II, we briefly describe the relevant schemes developed in the LC hybrid approach. In Sec. III, we propose a new SR exchange functional, which serves as suitable basis functionals for systematically generating accurate LC hybrid MGGA functionals. The performance of the ωM05-D functional is compared with other functionals in Sec. IV (on the training set), and in Sec. V (on some test sets). In Sec. VI, we give our conclusions.
II. RATIONALES OF LC HYBRID SCHEMES

For the LC hybrid schemes, one first defines the long-range and short-range operators to partition the Coulomb operator. The most popular type of splitting operator used is the standard error function (erf),

\[
\frac{1}{r_{12}} = \frac{\text{erf}(\omega r_{12})}{r_{12}} + \frac{\text{erfc}(\omega r_{12})}{r_{12}},
\]

where \( r_{12} \equiv |\mathbf{r}_{12}| = |\mathbf{r}_1 - \mathbf{r}_2| \) (atomic units are used throughout this paper). On the right hand side of Eq. (1), the first term is long-ranged, while the second term is short-ranged. The parameter \( \omega \) defines the range of these operators.

In this work, we employ the erf/erfc partition, and use the following expression (as suggested in the recent LC hybrid schemes [35, 36, 49]) for the LC hybrid functionals (\( c_x \) is a fractional number to be determined):

\[
E^{\text{LC-DFA}}_{xc} = E^{\text{LR-HF}}_x + c_x E^{\text{SR-HF}}_x + (1 - c_x) E^{\text{SR-DF}}_x + E^{\text{DFA}}_c,
\]

where \( E^{\text{LR-HF}}_x \), the LR HF exchange, is computed by the occupied KS orbitals \( \psi_{\sigma_i}^*(\mathbf{r}) \) with the LR operator,

\[
E^{\text{LR-HF}}_x = -\frac{1}{2} \sum_{\sigma}^{\text{occ.}} \sum_{i,j} \int \int \psi_{\sigma_i}^*(\mathbf{r}_1) \psi_{\sigma_j}^*(\mathbf{r}_2) \text{erf}(\omega r_{12}) \frac{\psi_{\sigma_j}(\mathbf{r}_1) \psi_{\sigma_i}(\mathbf{r}_2)}{r_{12}} \, d\mathbf{r}_1 \, d\mathbf{r}_2,
\]

\( E^{\text{SR-HF}}_x \), the SR HF exchange, is computed similarly to the above but with the SR operator,

\[
E^{\text{SR-HF}}_x = -\frac{1}{2} \sum_{\sigma}^{\text{occ.}} \sum_{i,j} \int \int \psi_{\sigma_i}^*(\mathbf{r}_1) \psi_{\sigma_j}^*(\mathbf{r}_2) \text{erfc}(\omega r_{12}) \frac{\psi_{\sigma_j}(\mathbf{r}_1) \psi_{\sigma_i}(\mathbf{r}_2)}{r_{12}} \, d\mathbf{r}_1 \, d\mathbf{r}_2,
\]

\( E^{\text{SR-DF}}_x \) is the SR exchange approximated by DFAs, and \( E^{\text{DFA}}_c \) is the correlation functional the same as that of the full Coulomb interaction.

In view of the \( E^{\text{LC-DFA}}_{xc} \) in Eq. (2), as \( E^{\text{LR-HF}}_x \) and \( E^{\text{SR-HF}}_x \) are well defined, and accurate approximations for \( E^{\text{DFA}}_c \) are widely available, the accuracy of \( E^{\text{SR-DF}}_x \) is thus closely related to the accuracy of a LC hybrid functional [35, 36]. The analytical form of the SR LDA (the simplest SR DFA) exchange functional \( E^{\text{SR-LDA}}_x \) can be obtained by the integration of the square of the LDA density matrix with the SR operator [50],

\[
E^{\text{SR-LDA}}_x = \sum_{\sigma} \int e^{\text{SR-LDA}}_{x\sigma}(\rho_{\sigma}) \, d\mathbf{r}.
\]

Here, \( e^{\text{SR-LDA}}_{x\sigma}(\rho_{\sigma}) \) is the SR LDA exchange energy density for \( \sigma \)-spin,

\[
e^{\text{SR-LDA}}_{x\sigma}(\rho_{\sigma}) = e^{\text{LDA}}_{x\sigma} F(a_{\sigma}),
\]

where

\[
e^{\text{LDA}}_{x\sigma}(\rho_{\sigma}) = -\frac{3}{2} \left( \frac{3}{4\pi} \right)^{1/3} \rho_{\sigma}^{1/3}(\mathbf{r})
\]
is the LDA exchange energy density for $\sigma$-spin, $k_{F\sigma} \equiv (6\pi^2 \rho_\sigma(\mathbf{r}))^{1/3}$ is the local Fermi wave vector, and $a_\sigma \equiv \omega/(2k_{F\sigma})$ is a dimensionless parameter controlling the value of the attenuation function $F(a_\sigma)$,

$$F(a_\sigma) = 1 - \frac{8}{3}a_\sigma \left[ \sqrt{\pi} \text{erf} \left( \frac{1}{2a_\sigma} \right) - 3a_\sigma + 4a_\sigma^3 + (2a_\sigma - 4a_\sigma^3) \exp \left( -\frac{1}{4a_\sigma^2} \right) \right]. \quad (8)$$

To develop a possible SR DFA exchange functional $E_{x\sigma}^{\text{SR-DFA}}$ based on the knowledge of a DFA exchange functional $E_{x\sigma}^{\text{DFA}}$, there are three schemes as follows. Consider the general expression of DFA exchange functional, which is

$$E_{x\sigma}^{\text{DFA}} = \sum_\sigma \int e^{LDA}_{x\sigma}(\rho_\sigma) F_{x\sigma}^{\text{DFA}} d\mathbf{r}, \quad (9)$$

$F_{x\sigma}^{\text{DFA}}$ is the DFA enhancement factor for $\sigma$-spin. Depending on the type of DFA, $F_{x\sigma}^{\text{DFA}} = 1$ for a LDA, $F_{x\sigma}^{\text{DFA}} = F_{x\sigma}^{\text{GGA}}(\rho_\sigma, \nabla \rho_\sigma)$ for a GGA, $F_{x\sigma}^{\text{DFA}} = F_{x\sigma}^{\text{MGGA}}(\rho_\sigma, \nabla \rho_\sigma, \tau_\sigma)$ for a meta-GGA, where $\rho_\sigma(\mathbf{r})$ is the spin density, $\nabla \rho_\sigma(\mathbf{r})$ is the spin density gradient, and

$$\tau_\sigma = \frac{1}{2} \sum_{i,\text{occ.}} |\nabla \psi_{i\sigma}|^2 \quad (10)$$
is the spin kinetic energy density.

The first scheme was proposed by Iikura, Tsuneda, Yanai, and Hirao (ITYH) \cite{27, 28, 33}, where $E_{x\sigma}^{\text{SR-DFA}}$ can be obtained by substituting a modified Fermi wave vector,

$$k_\sigma = \frac{k_{F\sigma}}{\sqrt{F_{x\sigma}^{\text{DFA}}}} \quad (11)$$

into SR exchange energy density of Eq. (6), which \textit{a priori} produces $E_{x\sigma}^{\text{SR-DFA}}$ from any $E_{x\sigma}^{\text{DFA}}$, and reduces nicely to $E_{x\sigma}^{\text{SR-LDA}}$ from a $E_{x\sigma}^{\text{LDA}}$. Although the ITYH scheme possesses an admirable simplicity, some of its deficiencies (which potentially limit its accuracy) have been found \cite{51}.

The second scheme was proposed by Vydrov, Heyd, Krukau, and Scuseria (VHKS) \cite{31, 32}, where for a given spherically-averaged exchange hole $h_{x\sigma}^{\text{DFA}}(\mathbf{r}, r_{12})$, $E_{x\sigma}^{\text{SR-DFA}}$ is evaluated as

$$E_{x\sigma}^{\text{SR-DFA}} = 2\pi \int \rho(\mathbf{r}) d\mathbf{r} \int_0^\infty \text{erfc}(\omega r_{12}) h_{x\sigma}^{\text{DFA}}(\mathbf{r}, r_{12}) r_{12} dr_{12}. \quad (12)$$

The pivot of this scheme is the engineering of the DFA exchange hole. The GGA model exchange hole of Ernzerhof and Perdew \cite{52} (EP) provides a framework for modeling any GGA exchange hole. It has made considerable appearances in real applications after parametrization to reproduce the Perdew, Burke, and Ernzerhof (PBE) GGA \cite{53}. In 2008, Henderson, Janesko, and Scuseria \cite{51} (HJS) proposed another general model for the spherically averaged exchange hole corresponding to a GGA exchange functional, based on the work of EP. The HJS model improves upon the EP model by precisely reproducing the energy of the parent GGA, and by enabling fully analytic evaluation of range-separated hybrid density functionals. For meta-GGA, the TPSS exchange and correlation hole
models have been “reverse-engineered” \[54\]. However, the resulting LC-TPSS functional (a LC hybrid MGGA) has no satisfactory long-range correction effect \[31\].

The third scheme was proposed by Chai and Head-Gordon (CHG) \[35, 36\], where $E_{x}^{SR-DA}$ is evaluated as

$$E_{x}^{SR-DA} = \sum_{\sigma} \int e_{x\sigma}^{SR-LDA} (\rho_{\sigma}) F_{x\sigma}^{DA} d\mathbf{r}.$$  \hspace{1cm} (13)

This simple scheme is expected to work well for a small $\omega$. For highly parametrized $E_{x}^{DA}$, such as the B97 \[40\], M05 \[18\], and M08 \[26\] functionals, the CHG scheme is particularly attractive due to its simplicity. However, how large is not too large for the $\omega$ suitable for the CHG scheme? In the following sections, we will compare the performance of two new LC hybrid MGGA-D functionals, where one is developed by the CHG scheme, while the other is developed by a new scheme provided in this work, and our results help to answer the above question.

### III. LC HYBRID MGGA-D FUNCTIONALS

In this section, we introduce our new LC hybrid MGGA-D functionals. Note that LC-TPSS has been developed by utilizing the TPSS exchange hole (based on the VHKS scheme) \[31\], but it is found that LC-TPSS does not benefit much by admixture of HF exchange. The M11 functional \[49\] has been developed based on the extension of a global hybrid MGGA functional, M08 \[26\], to LC-DFT, following the CHG scheme \[35\].

Parallel to the strategy of the $\omega$B97 series \[35, 36\], we choose to modify the M05 functional. The M05 functional is a global hybrid MGGA functional with a powerful form \[18, 19\], and our work is based on modifying this functional. Its exchange part consists of the PBE exchange functional and a reasonable kinetic-energy-density enhancement factor. The PBE exchange is a theoretically sound starting point because it satisfies the correct UEG limit and also has reasonable behavior at large values of the reduced spin density gradient $s_{\sigma}$.

To satisfy the UEG limit of SR exchange, we replace the PBE exchange energy density $e_{x\sigma}^{PBE} (\rho_{\sigma}, \nabla \rho_{\sigma})$ with the SR-PBE exchange energy density $e_{x\sigma}^{SR-PBE} (\rho_{\sigma}, \nabla \rho_{\sigma})$ generated by the HJS model exchange hole (based on the VHKS scheme), whose virtues are indicated in Sec. II. To achieve a flexible functional form, we retain the kinetic-energy-density enhancement factor (similar to the CHG scheme). We denote this resulting functional as SR-M05 (short-range M05) exchange, as it reduces to the M05 exchange at $\omega = 0$.

$$E_{x}^{SR-M05} = \sum_{\sigma} \int e_{x\sigma}^{SR-PBE} (\rho_{\sigma}, \nabla \rho_{\sigma}) f(w_{\sigma}) d\mathbf{r},$$  \hspace{1cm} (14)

where $f(w_{\sigma})$ is the kinetic-energy-density enhancement factor,

$$f(w_{\sigma}) = \sum_{i=0}^{m} a_{i} w_{\sigma}^{i}. $$  \hspace{1cm} (15)
$w_\sigma$ is a function of $t_\sigma$, and $t_\sigma$ is a function of the kinetic energy density $\tau_\sigma$ of electrons with spin $\sigma$, as designed by Becke \[23\],

$$w_\sigma = (t_\sigma - 1)/(t_\sigma + 1),$$  \hspace{1cm} (16)

where

$$t_\sigma = \frac{\tau^{\text{LDA}}_\sigma}{\tau_\sigma},$$  \hspace{1cm} (17)

$$\tau^{\text{LDA}}_\sigma \equiv \frac{3}{10} \left( 6\pi^2 \right)^{2/3} \frac{s^{5/3}}{\rho_\sigma}.$$  \hspace{1cm} (18)

In general, the enhancement factor should be $\omega$-dependent. But from the works of LC-TPSS \[31\] and M11 \[49\], the optimal $\omega$ for a LC hybrid MGGA is expected to be small as well. For a sufficiently small $\omega$ value, our proposed functional form, inspired by the VHKS and CHG schemes, should be a good approximation.

We use the same form for the correlation functional as the M05 correlation functional, which can be decomposed into same-spin $E^{\text{M05}}_{c \sigma \sigma}$ and opposite-spin $E^{\text{M05}}_{c \alpha \beta}$ components,

$$E^{\text{M05}}_c = \sum_\sigma E^{\text{M05}}_{c \sigma \sigma} + E^{\text{M05}}_{c \alpha \beta}.$$  \hspace{1cm} (19)

For the opposite-spin terms,

$$E^{\text{M05}}_{c \alpha \beta} = \int \epsilon^{\text{LDA}}_{c \alpha \beta} g_{\alpha \beta}(s^2_{av}) dr,$$  \hspace{1cm} (20)

$$g_{\alpha \beta}(s^2_{av}) = \sum_{i=0}^{n} c_{\alpha \beta, i} u_{\alpha \beta}^i,$$  \hspace{1cm} (21)

$$u_{\alpha \beta} = \frac{\gamma_{\alpha \beta} s^2_{av}}{1 + \gamma_{\alpha \beta} s^2_{av}},$$  \hspace{1cm} (22)

$$\gamma_{\alpha \beta} = 0.0062,$$  \hspace{1cm} (23)

$$s^2_{av} = \frac{1}{2}(s^2_\alpha + s^2_\beta),$$  \hspace{1cm} (24)

and for the same-spin terms,

$$E^{\text{M05}}_{c \sigma \sigma} = \int \epsilon^{\text{LDA}}_{c \sigma \sigma} g_{\sigma \sigma}(s^2_{\sigma}) (1 - \frac{\tau^W_{\sigma}}{\tau_\sigma}) dr,$$  \hspace{1cm} (25)

$$g_{\sigma \sigma}(s^2_{\sigma}) = \sum_{i=0}^{n} c_{\sigma \sigma, i} u_{\sigma \sigma}^i,$$  \hspace{1cm} (26)

$$u_{\sigma \sigma} = \frac{\gamma_{\sigma \sigma} s^2_{\sigma}}{1 + \gamma_{\sigma \sigma} s^2_{\sigma}},$$  \hspace{1cm} (27)

$$\gamma_{\sigma \sigma} = 0.06.$$  \hspace{1cm} (28)

$1 - \tau^W_{\sigma}/\tau_\sigma$ is a self-interaction correction factor proposed by Becke, \[22\] in which $\tau^W_{\sigma}$ is the von Weizsäcker kinetic energy density \[55\] given by

$$\tau^W_{\sigma} = \frac{|\nabla \rho_\sigma|^2}{8 \rho_\sigma}.$$  \hspace{1cm} (29)
In a one-electron case, \( \tau_\sigma = \tau_\sigma^W \), so Eq. (25) vanishes in any one-electron system. The correlation energy densities \( e_{c_{\alpha\beta}}^{\text{LDA}} \) and \( e_{c_{\sigma\sigma}}^{\text{LDA}} \) are derived from the Perdew-Wang parametrization of the LDA correlation energy [56], using the approach of Stoll et al. [57],

\[
e_{c_{\alpha\beta}}^{\text{LDA}}(\rho_\alpha, \rho_\beta) = e_{c_{\alpha\beta}}^{\text{LDA}}(\rho_\alpha, \rho_\beta) - e_{c_{\alpha\beta}}^{\text{LDA}}(\rho_\alpha, 0) - e_{c_{\alpha\beta}}^{\text{LDA}}(0, \rho_\beta),
\]

(30)

\[
e_{c_{\sigma\sigma}}^{\text{LDA}} = e_{c_{\sigma\sigma}}^{\text{LDA}}(\rho_\sigma, 0).
\]

(31)

Based on the above functional expansions, we propose a new LC hybrid MGGA functional, \( \omega\text{M05-D} \). It contains a fraction of the SR HF exchange,

\[
E_{xc}^{\omega\text{M05-D}} = E_x^{\text{LR-HF}} + c_x E_x^{\text{SR-HF}} + E_x^{\text{SR-M05}} + E_x^{\text{M05}}.
\]

(32)

We enforce the exact UEG limit for the \( \omega\text{M05-D} \) functional by imposing the following constraints:

\[
e_{c_{\sigma\sigma},0} = 1,
\]

(33)

\[
e_{c_{\alpha\beta},0} = 1,
\]

(34)

and

\[
a_0 + c_x = 1.
\]

(35)

Following the general form of the DFT-D scheme [43], our total energy

\[
E_{\text{DFT-D}} = E_{\text{KS-DFT}} + E_{\text{disp}}
\]

(36)

is computed as the sum of a KS-DFT part and an empirical atomic-pairwise dispersion correction. We choose to use the same form of unscaled dispersion correction as implemented in \( \omega\text{B97X-D} \) [36],

\[
E_{\text{disp}} = - \sum_{i=1}^{N_{\text{at}}-1} \sum_{j=i+1}^{N_{\text{at}}} \frac{C_6^{ij}}{R_{ij}^6} f_{\text{damp}}(R_{ij}),
\]

(37)

where \( N_{\text{at}} \) is the number of atoms in the system, \( C_6^{ij} \) is the dispersion coefficient for atom pair \( ij \), and \( R_{ij} \) is an interatomic distance. The damping function,

\[
f_{\text{damp}}(R_{ij}) = \frac{1}{1 + a(R_{ij}/R_r)^{-12}}
\]

(38)

enforces the conditions of zero dispersion correction at short interatomic separations and correct asymptotic pairwise vDW potentials. Here, \( R_r \) is the sum of vDW radii of the atomic pair \( ij \), and the only non-linear parameter, \( a \), controls the strength of dispersion corrections.
To achieve an optimized functional for well-balanced performance across typical applications, we use the same diverse training set described in Ref. [35], which contains 412 accurate experimental and accurate theoretical results, including the 18 atomic energies from the H atom to the Ar atom [58], the atomization energies of the G3/99 set (223 molecules) [59–61], the ionization potentials (IPs) of the G2-1 set [62] (40 molecules, excluding SH$_2$(2$^2$A$_1$) and N$_2$(2$^2$Π) cations due to the known convergence problems for semilocal density functionals [60]), the electron affinities (EAs) of the G2-1 set (25 molecules), the proton affinities (PAs) of the G2-1 set (8 molecules), the 76 barrier heights of the NHTBH38/04 and HTBH38/04 sets [15, 63], and the 22 noncovalent interactions of the S22 set [64]. The S22 data is weighted ten times more than the others. All the parameters in $\omega$M05-D are determined self-consistently by a least-square fitting procedure described in Ref. [35]. For the non-linear parameter optimization, we focus on a range of possible $\omega$ values (0.0, 0.1, 0.2, 0.3, and 0.4 Bohr$^{-1}$), and optimize the corresponding $a$ values in the steps described in Ref. [36].

M05 and M05-2X [18, 19] both used $m$=11 in Eq. (15) and $n$=4 in Eqs. (21) and (26). However, during the optimization procedure of $\omega$M05-D, we found that the statistical errors are close for $m$=10 and $m$=11, while the one with $m$=11 has parameters significantly larger. A recent study by Wheeler and Houk has shown that large magnitude of the parameters in Eq. (15) may result in large grid errors [65]. Moreover, the use of large parameters increases the possibility of convergence difficulty as well as the over-fitting effects. Thus, we choose $m$=10 instead of 11 in Eq. (15). The optimized parameters of the $\omega$M05-D functional are given in Table I in which the $\omega$ value is same as that of $\omega$B97X-D, while the fraction of SR HF exchange, $c_x$, is larger than that of $\omega$B97X-D (≈ 0.22). This helps to reduce the self-interaction error (SIE) of the functional, as can be seen in Sec. V.

We also tried a simple model (based on the CHG scheme), where the SR-PBE exchange energy density $\epsilon_{x}\sigma^{SR-PBE}(\rho_\sigma, \nabla \rho_\sigma)$ used in Eq. (14) is substituted with $\epsilon_{x}\sigma^{SR-LDA}(\rho_\sigma)F_{x}^{PBE}(s_\sigma)$, that is, the SR LDA exchange energy density in Eq. (6) multiplied by the PBE enhancement factor. We tried this because the mathematical form of the latter is significantly simpler than that of the former, and is the model on which M11 based. The parametrization is the same for this simple model, which we denoted by $\omega$M05s-D. Compared to $\omega$M05-D, the optimal $\omega$ value is also 0.2 bohr$^{-1}$, but the corresponding optimal $a$ value is found to be 100 and the linear parameters are also larger.

IV. RESULTS FOR THE TRAINING SET

All calculations are performed with a development version of Q-CHEM 3.2 [66]. Spin-restricted theory is used for singlet states and spin-unrestricted theory for others, unless noted otherwise. For the binding energies of the weakly bound systems, the counterpoise correction [67] is employed to reduce basis set superposition error (BSSE).

Results for the training set are computed using the 6-311++G(3df,3pd) basis set with the fine grid, EML(75,302),
TABLE I. Optimized parameters for $\omega_{\text{M05-D}}$. Here, the non-linear parameter $a$ is defined in Eq. (38), and others are defined in Eq. (32)

| $a$ | 30.0 |
|-----|-----|
| $\omega$ | 0.2 Bohr$^{-1}$ |
| $c_x$ | 0.369592 |

| $i$ | $a_i$ | $c_{\alpha\beta,i}$ | $c_{\sigma\sigma,i}$ |
|-----|-------|-------------------|-------------------|
| 0   | 0.630408 | 1.00000           | 1.00000           |
| 1   | -0.219121 | -0.95491         | -5.26863          |
| 2   | -0.14411  | 12.138            | 17.9935           |
| 3   | 1.27732   | -35.1041          | -17.6408          |
| 4   | -1.59959  | 19.5804           | 0.625687          |
| 5   | -5.94702  |                   |                   |
| 6   | 13.5822   |                   |                   |
| 7   | 10.5048   |                   |                   |
| 8   | -28.7168  |                   |                   |
| 9   | -6.89761  |                   |                   |
| 10  | 19.0574   |                   |                   |

consisting of 75 Euler-Maclaurin radial grid points $^{68}$ and 302 Lebedev angular grid points $^{69}$. The error for each entry is defined as error = theoretical value − reference value. The notation used for characterizing statistical errors is as follows: mean signed errors (MSEs), mean absolute errors (MAEs), root-mean-square (rms) errors, maximum negative errors (Max(−)), and maximum positive errors (Max(+)).

First, we show the results of the first iteration of fitting procedure, comparing the new LC scheme with the CHG scheme (the simple model) for $\omega=0.1$, 0.2, 0.3 and 0.4 bohr$^{-1}$. We optimize $\omega\text{M05}$ and $\omega\text{M05s}$ using the corresponding $\omega\text{PBE}$ and $\omega\text{PBEs}$ orbitals, and denote these optimized functionals as $\omega\text{M05}^*$ and $\omega\text{M05s}^*$. The statistical errors are believed to be quite close to those obtained self-consistently. As can be seen in Table III, the difference between the performance of $\omega\text{M05}^*$ and $\omega\text{M05s}^*$ is noticeable for $\omega=0.2$ bohr$^{-1}$, and becomes larger for a larger $\omega$ value. Therefore, a LC hybrid MGGA functional with a larger $\omega$ value (such as M11 with $\omega=0.25$ bohr$^{-1}$) may perform better with our new scheme than with the CHG scheme.

In subsequent iterations, we include the dispersion corrections, increase the training weight of S22 set, and found the functionals optimized with $\omega=0.2$ bohr$^{-1}$. To view the effect of the long-range correction and the dispersion
corrections, we also consider the functional form M05 and M05-D. The latter is the limiting case where \( \omega = 0 \) for \( \omega \text{M05-D} \), of which the corresponding optimal \( a \) value is found to be 2. We reoptimize M05 and M05-D functionals on the same training set using the M05-2X orbitals, truncate their functional expansions at the same orders \( m=10 \) and \( n=4 \), and denote these two reoptimized functionals as M05* and M05-D*. Just like the \( \omega \text{B97X} \) functional without dispersion correction, all data in the training set are equally weighted in the least-squares fitting for M05*.

The overall performance of our new \( \omega \text{M05-D} \) is compared with the trial simple model \( \omega \text{M05s-D} \), M05-D*, M05* and M05-2X \[19\], as well as existing \( \omega \text{B97X-D} \) (a LC hybrid GGA-D) \[36\]. Note that M05 \[18\] and M05-2X share the same functional form, but the former is distracted to deal with transition-metal compounds, so the latter should be our concern. In the \( \omega \text{B97} \) series, \( \omega \text{B97X-D} \) has the closest relationship to \( \omega \text{M05-D} \), while \( \omega \text{B97} \) and \( \omega \text{B97X} \), developed without dispersion corrections, are expected to perform poorly for noncovalent interactions.

In Table III, the first comparison (\( \omega \text{M05-D} \) vs. \( \omega \text{M05s-D} \)) partially determines the choice of our proposed functional. Although \( \omega \text{M05-D} \) performs worse than \( \omega \text{M05s-D} \) for HTBH, the overall performance of \( \omega \text{M05-D} \) in the training set is the best.

A second comparison between \( \omega \text{M05-D} \) and M05-D* indicates that the exact long-range exchange indeed leads to an overall improvement to MGGA, although not as large as that to GGA \[31, 35, 36\]. The third comparison is between M05-D* and M05*. The cooperation of the training weight and the empirical dispersion corrections leads to a significant improvement in the results for noncovalent interactions (the S22 data) and a modest overall change. Recently, there have been the updated reference values for the S22 set \[70\]. We have also examined the performance of \( \omega \text{M05-D} \) against the updated S22 reference values. As shown in the supplementary material \[71\], the overall performance of the functional against the updated reference values is similar to that against the original ones.

V. RESULTS FOR THE TEST SETS

To test the performance of \( \omega \text{M05-D} \) outside its training set, we also evaluate its performance on various test sets involving 48 atomization energies in the G3/05 test set \[72\], 30 chemical reaction energies taken from the NHTBH38/04 and HTBH38/04 databases \[15, 63\], 29 noncovalent interactions \[63, 64\], 166 optimized geometry properties of covalent systems \[73\], 12 intermolecular bond lengths \[64\], 4 dissociation curves of symmetric radical cations as well as three new databases, consisting of 131 vertical IPs, 115 vertical EAs and 115 fundamental gaps. For excitation energies, we perform TDDFT calculations for 19 valence excitation energies, 23 Rydberg excitation energies and one long-range charge transfer excitation curve of two well-separated molecules. Each EA can be evaluated by two different ways, and each fundamental gap can be evaluated by three different ways, so there are a total of 1038 pieces of data in the test sets, which are larger and more diverse than the training set. Unspecified
TABLE II. Comparisons between the $\omega M05^*$ and $\omega M05s^*$ functionals (defined in the text) for different $\omega$ values. Statistical errors are in kcal/mol.

| System | $\omega$ (Bohr$^{-1}$) | Error | $\omega M05^*$ | $\omega M05s^*$ | $\omega M05^*$ | $\omega M05s^*$ | $\omega M05^*$ | $\omega M05s^*$ |
|--------|------------------------|-------|--------------|----------------|--------------|----------------|--------------|----------------|
|        | 0.1                    |       | 0.1          | 0.2            | 0.2          | 0.3            | 0.3          | 0.4            | 0.4          |
| Atoms  | MSE                    | -0.15 | 0.24         | 0.05           | 0.63         | 0.23           | 0.97         | 0.46           | 1.33         |
|        | MAE                    | 2.02  | 2.09         | 1.81           | 2.35         | 2.00           | 3.36         | 3.22           | 5.05         |
| G3/99  | MSE                    | 0.06  | 0.09         | 0.05           | 0.03         | -0.04          | -0.12        | -0.18          | -0.27        |
|        | MAE                    | 1.77  | 1.79         | 1.66           | 1.76         | 1.78           | 2.02         | 2.10           | 2.35         |
| IP     | MSE                    | -0.58 | -1.48        | -0.84          | -1.36        | -0.38          | -0.32        | 0.30           | 0.73         |
|        | MAE                    | 2.75  | 3.06         | 2.81           | 3.08         | 2.68           | 2.81         | 2.64           | 2.79         |
| EA     | MSE                    | -1.50 | -1.70        | -1.29          | -1.15        | -0.94          | -0.70        | -0.64          | -0.39        |
|        | MAE                    | 2.50  | 2.56         | 2.33           | 2.22         | 2.07           | 1.97         | 1.98           | 1.91         |
| PA     | MSE                    | -1.65 | -2.68        | -1.49          | -2.71        | -1.07          | -2.11        | -0.78          | -1.54        |
|        | MAE                    | 1.87  | 2.68         | 1.83           | 2.82         | 1.79           | 2.53         | 1.86           | 2.43         |
| NHTBH  | MSE                    | -1.26 | -1.09        | -0.68          | -0.39        | 0.08           | 0.40         | 0.85           | 1.17         |
|        | MAE                    | 1.98  | 1.82         | 1.51           | 1.40         | 1.46           | 1.67         | 1.71           | 1.95         |
| HTBH   | MSE                    | -1.96 | -1.95        | -1.95          | -1.68        | -1.61          | -1.24        | -1.21          | -0.84        |
|        | MAE                    | 2.19  | 2.08         | 2.12           | 1.84         | 1.95           | 1.56         | 1.86           | 1.47         |
| S22    | MSE                    | 2.65  | 1.91         | 1.80           | 1.06         | 1.01           | 0.56         | 0.45           | 0.26         |
|        | MAE                    | 2.65  | 1.91         | 1.80           | 1.06         | 1.02           | 0.67         | 0.71           | 0.63         |
| All    | MSE                    | -0.31 | -0.42        | -0.30          | -0.35        | -0.21          | -0.18        | -0.11          | -0.02        |
|        | MAE                    | 2.03  | 2.03         | 1.86           | 1.90         | 1.84           | 2.01         | 2.06           | 2.28         |
TABLE III. Statistical errors (in kcal/mol) of the training set. The M05-D* and M05* functionals are defined in the text.

M05-2X was not particularly parametrized using this training set.

| System | Error | ωM05-D | ωM05s-D | M05-D* | M05* | M05-2X | ωB97X-D |
|--------|-------|--------|---------|--------|------|--------|---------|
| Atoms  | MSE   | 0.37   | 0.83    | 0.18   | -0.48| -3.01  | -0.05   |
|        | MAE   | 2.02   | 2.28    | 2.61   | 1.98 | 5.10   | 2.57    |
| G3/99  | MSE   | -0.03  | -0.03   | -0.10  | -0.05| 2.01   | -0.24   |
|        | MAE   | 1.62   | 1.73    | 1.78   | 1.78 | 3.65   | 1.93    |
| IP     | MSE   | -0.80  | -1.33   | 0.06   | 0.27 | 1.10   | 0.19    |
|        | MAE   | 2.86   | 3.04    | 2.84   | 2.51 | 3.35   | 2.74    |
| EA     | MSE   | -1.02  | -0.98   | -0.54  | -0.84| -0.23  | 0.07    |
|        | MAE   | 2.12   | 2.13    | 2.13   | 2.35 | 2.48   | 1.91    |
| PA     | MSE   | -1.48  | -2.66   | -0.94  | -1.76| -1.26  | 1.42    |
|        | MAE   | 2.10   | 3.07    | 1.31   | 2.17 | 1.51   | 1.50    |
| NHTBH  | MSE   | -0.94  | -0.59   | -1.38  | -1.32| 0.13   | -0.45   |
|        | MAE   | 1.57   | 1.53    | 2.04   | 2.08 | 1.75   | 1.51    |
| HTBH   | MSE   | -2.82  | -2.33   | -2.95  | -1.77| -0.65  | -2.57   |
|        | MAE   | 2.83   | 2.37    | 3.08   | 2.14 | 1.51   | 2.70    |
| S22    | MSE   | -0.01  | -0.01   | 0.04   | 3.46 | 0.73   | -0.08   |
|        | MAE   | 0.27   | 0.21    | 0.23   | 3.46 | 0.87   | 0.21    |
| All    | MSE   | -0.51  | -0.49   | -0.49  | -0.21| 1.02   | -0.36   |
|        | MAE   | 1.83   | 1.89    | 1.99   | 2.05 | 3.05   | 1.96    |
| System  | Error | $\omega$M05-D | $\omega$M05s-D | M05-2X | $\omega$B97X-D |
|---------|-------|---------------|----------------|--------|----------------|
| G3/05   | MSE   | -0.85         | -1.67          | 0.00   | 0.25           |
|         | MAE   | 3.21          | 3.79           | 5.24   | 3.02           |
| RE      | MSE   | -0.58         | -0.65          | -0.86  | -0.24          |
|         | MAE   | 1.49          | 1.32           | 1.65   | 1.63           |
| Non-covalent | MSE   | -0.11         | -0.05          | 0.50   | -0.15          |
|         | MAE   | 0.31          | 0.30           | 0.61   | 0.43           |
| All     | MSE   | -0.58         | -0.95          | -0.11  | 0.01           |
|         | MAE   | 1.94          | 2.15           | 2.98   | 1.93           |

detailed information of the test sets as well as the basis sets, and numerical grids used is given in Ref. [35].

A. Atomization Energies, Reaction Energies, and Noncovalent Interactions

Table [IV] summarized the general energetic results in the same way as in Ref. [36], for convenience of further comparisons. Since the 30 chemical reaction energies are taken from the NHTBH38/04 and HTBH38/04 databases calculated in Table [III], the EML(75,302) grid is used. In Table [IV] the comparison between $\omega$M05-D and $\omega$M05s-D shows noticeable difference in atomization energies, and makes great influence on the choice of our proposed functional.

B. Equilibrium Geometries

Satisfactory predictions of molecular geometries of covalent and non-covalent systems by density functionals are necessary for practical use. For covalent systems, we perform geometry optimizations for each functional on the equilibrium experimental test set (EXTS) [73], while for non-covalent systems, we compute the intermolecular bond lengths of 12 weakly bound complexes taken from the S22 set [64], using 6-311++G(3df,3pd) basis set with the EML(75,302) grid. As shown in Table [V] performance of all the hybrid functionals in predicting optimized geometries of EXTS is similar, while the performance of simple model ($\omega$M05s-D) is somewhat worse for the
TABLE V. Statistical errors (in Å) of EXTS (Ref. [73]) and bond lengths of 12 weakly bound complexes from the S22 set (Ref. [64]). The results of ωB97X-D are taken from Ref. [36].

| System       | Error | ωM05-D | ωM05s-D | M05-2X | ωB97X-D |
|--------------|-------|--------|---------|--------|---------|
| MSE          | 0.003 | 0.001  | -0.004  | -0.002 |
| MAE          | 0.010 | 0.009  | 0.009   | 0.009  |
| EXTS (166)   | rms   | 0.019  | 0.014   | 0.014  | 0.013   |
|              | Max(−) | -0.081 | -0.083  | -0.082 | -0.078  |
|              | Max(+) | 0.177  | 0.067   | 0.054  | 0.055   |
| MSE          | -0.041| -0.069 | -0.021  | -0.044 |
| MAE          | 0.061 | 0.078  | 0.062   | 0.064  |
| Weak (12)    | rms   | 0.083  | 0.102   | 0.080  | 0.085   |
|              | Max(−) | -0.189 | -0.195  | -0.165 | -0.198  |
|              | Max(+) | 0.043  | 0.029   | 0.140  | 0.056   |

intermolecular bond lengths. We decide our proposed model to be ωM05-D in this subsection. For brevity, the performance of ωM05s-D will not be shown for subsequent calculations.

C. Dissociation of Symmetric Radical Cations

Common semilocal functionals are generally accurate for systems near equilibrium. However, due to considerable self-interaction errors in semilocal functionals, spurious fractional charge dissociation occurs [32, 74, 75]. This situation becomes amplified for symmetric charged radicals X2+, such as H2+, He2+, Ne2+, and Ar2+. Gräfenstein and coworkers have obtained qualitatively correct result for these systems [76, 77] using self-interaction-corrected DFT proposed by Perdew and Zunger [78], and confirmed that the errors of standard DFT methods should be dominated by the SIEs.

We perform unrestricted calculations with the aug-cc-pVQZ basis set and a high-quality EML(250,590) grid. The DFT results are compared with results from HF theory, and the very accurate CCSD(T) theory [79, 80]. The HF method is exact in Fig. 1 and gives qualitatively correct results from Fig. 2 to Fig. 4. Although ωM05-D has the same amount of LR HF exchange as ωB97X-D, the larger fraction of SR HF exchange included in ωM05-D helps to reduce its remaining SIE. Therefore, the error of ωM05-D is smaller than that of ωB97X-D, especially for larger cations (e.g. Ne2+ and Ar2+). The global hybrid functional M05-2X exhibits the undesirable X2+ dissociation.
FIG. 1. Dissociation curve of \( \text{H}_2^+ \). Zero level is set to \( \text{E}(\text{H})+\text{E}(\text{H}^+) \) for each method.

curves, displaying a spurious energy barrier at intermediate bond length \( R \).

**D. Frontier Orbital Energies**

Let \( \text{IP}(N) \) be the ionization potential and \( \text{EA}(N) \) be the electron affinity of the \( N \)-electron system, which are defined as

\[
\text{IP}(N) = E_{N-1} - E_N, \tag{39}
\]

\[
\text{EA}(N) = E_N - E_{N+1}, \tag{40}
\]

respectively, with \( E_N \) being the total energy of \( N \)-electron system. For the exact DFT, the vertical ionization potential of a neutral molecule is identical to the minus HOMO (highest occupied molecular orbital) energy of the neutral molecule \([3, 81]\),

\[
\text{IP}(N) = -\epsilon_N(N), \tag{41}
\]

and the vertical electron affinity of a neutral molecule is identical to the minus HOMO energy of the anion (since \( \text{EA}(N) = \text{IP}(N+1) \) by definition),

\[
\text{EA}(N) = -\epsilon_{N+1}(N+1), \tag{42}
\]
where $\epsilon_M(N)$ is the $M$-th orbital energy of $N$-electron system. The vertical electron affinity of a neutral molecule may also be approximated by the minus LUMO (lowest unoccupied molecular orbital) energy of the neutral molecule, but it is proved that there exists a difference between the vertical EA and the minus LUMO energy,

$$\Delta_{xc} = \epsilon_{N+1}(N+1) - \epsilon_{N+1}(N),$$

where the difference $\Delta_{xc}$ arises from the discontinuity of exchange-correlation potentials [82–84]. Recent study shows that $\Delta_{xc}$ is close to zero for LC hybrid functionals [85], so the minus LUMO energy calculated by a LC hybrid functional should be close to the vertical EA.

To evaluate the performance of the functionals on the HOMO energy of the neutral molecule, we collect a new database, IP131, which consists of experimental vertical IPs of 18 atoms and 113 molecules in the experimental geometries. The geometries and most of the reference values are collected from the NIST database [86]. Other publications [87] are adopted for the experimental vertical IPs of some molecules. The DFT calculations are performed with 6-311++G(3df,3pd) basis and EML(75,302) grid. As can be seen in Table VI, $\omega$M05-D gives the best results. The global hybrid M05-2X gives the worst results here, due to its incorrect long-range XC-potential behavior.

To evaluate the performance of the functionals on the vertical electron affinity, we construct another database
FIG. 3. Dissociation curve of Ne$_2^+$. Zero level is set to E(Ne)+E(Ne$^+$) for each method.

called EA115, which consists of 18 atoms and 97 molecules. For the molecular geometries, it is a subset of IP131. Because experimental vertical EAs are not as widely available as experimental vertical IPs, the reference values of vertical EAs are obtained via the accurate CCSD(T) calculations (using Eq. (40)). The CCSD(T) correlation energies in the basis-set limit are extrapolated from calculations using the aug-cc-pVTZ and aug-cc-pVQZ basis sets [88]:

$$E_{XY}^\infty = \frac{E_{corr}^X X^3 - E_{corr}^Y Y^3}{X^3 - Y^3}, \quad (44)$$

where $X=3$ and $Y=4$ for the aug-cc-pVTZ and aug-cc-pVQZ basis, respectively. The electron affinities are evaluated in two different ways, as shown in Table VII for the minus HOMO energy of the anion, and Table VIII for the minus LUMO energy of the neutral molecule. Clearly, the LC hybrid functionals outperform the global hybrid M05-2X. The reference values and molecular geometries of IP131 and EA115 are given in the supplementary material [71] along with detailed DFT results.
FIG. 4. Dissociation curve of $\text{Ar}_2^+$. Zero level is set to $E(\text{Ar})+E(\text{Ar}^+)$ for each method.

TABLE VI. Statistical errors (in eV) for the IP131 database. Error is defined as $-\epsilon_N(N) - IP_{\text{vertical}}$. Experimental geometries and reference values are used for all molecules.

| System  | Error | $\omega$M05-D | M05-2X | $\omega$B97X-D |
|---------|-------|--------------|--------|---------------|
| atoms   | MSE   | -1.48        | -2.06  | -1.64         |
|         | MAE   | 1.48         | 2.06   | 1.64          |
|         | rms   | 1.74         | 2.16   | 1.98          |
| (18)    | MSE   | -0.68        | -1.23  | -0.92         |
|         | MAE   | 0.68         | 1.23   | 0.92          |
|         | rms   | 0.76         | 1.27   | 1.00          |
| molecules | MSE   | -0.79        | -1.34  | -1.02         |
|         | MAE   | 0.79         | 1.34   | 1.02          |
|         | rms   | 0.96         | 1.43   | 1.18          |
TABLE VII. Statistical errors (in eV) for the EA115 database. Error is defined as \(- \epsilon_{N+1}(N + 1) - E_{A_{vertical}}\). Experimental geometries and CCSD(T) reference values are used for all molecules.

| System     | Error | M05-D | M05-2X | B97X-D |
|------------|-------|-------|--------|--------|
| atoms      | MSE   | -0.46 | -1.21  | -0.53  |
|            | MAE   | 0.49  | 1.21   | 0.57   |
|            | rms   | 0.73  | 1.35   | 0.84   |
| moecules   | MSE   | -0.54 | -1.18  | -0.54  |
|            | MAE   | 0.55  | 1.18   | 0.56   |
|            | rms   | 0.80  | 1.32   | 0.82   |
| total      | MSE   | -0.53 | -1.18  | -0.54  |
|            | MAE   | 0.55  | 1.18   | 0.56   |
|            | rms   | 0.79  | 1.32   | 0.82   |

TABLE VIII. Statistical errors (in eV) of the minus LUMO energy of the neutral molecule for the EA115 database. Experimental geometries and CCSD(T) reference values are used for all molecules.

| System     | Error | M05-D | M05-2X | B97X-D |
|------------|-------|-------|--------|--------|
| atoms      | MSE   | -0.27 | 0.57   | -0.02  |
|            | MAE   | 0.73  | 1.02   | 0.74   |
|            | rms   | 0.92  | 1.12   | 0.89   |
| moecules   | MSE   | -0.24 | 0.60   | 0.05   |
|            | MAE   | 0.60  | 0.75   | 0.52   |
|            | rms   | 0.69  | 0.94   | 0.60   |
| total      | MSE   | -0.24 | 0.60   | 0.04   |
|            | MAE   | 0.62  | 0.79   | 0.55   |
|            | rms   | 0.73  | 0.97   | 0.65   |

E. Fundamental Gaps

The fundamental gap \(E_g\) of a molecule with \(N\) electrons is defined as

\[
E_g = \text{IP}(N) - \text{EA}(N).
\] (45)
Following Eqs. (39) and (40) for the definitions of IP and EA, three self-consistent field (SCF) calculations (for the neutral molecule, cation and anion) are required to obtain the fundamental gap of a molecule. Using Eq. (41) and (42), the fundamental gap of a molecule can also be obtained by two SCF calculations (for the neutral molecule and anion).

Following Janak’s theorem [89], the fundamental gap can be approximated by the HOMO-LUMO gap [84]

$$\Delta_{KS} = \epsilon_{N+1}(N) - \epsilon_N(N),$$

and we can obtain the fundamental gap of a system using only one calculation. But from Eqs. (41), (42), (43), (45), and (46), we know that there exists a difference between the fundamental gap and HOMO-LUMO gap,

$$E_g = \Delta_{KS} + \Delta_{xc}.$$ 

As previously mentioned, $\Delta_{xc}$ has been shown to be close to zero for LC hybrid functionals [85], so the HOMO-LUMO gap calculated by a LC hybrid functional should be close to the fundamental gap.

To evaluate the performance of the functionals on fundamental gap, we construct another database called FG115, which shares the same molecular geometries with the EA115 database. For consistency, the reference values of fundamental gaps are also obtained via the CCSD(T) calculations described in the last subsection (using Eqs. (39), (40), and (45)).

To examine the performance of density functionals, we evaluate the fundamental gaps using three different estimates, with 6-311++G(3df,3pd) basis and EML(75,302) grid. The results are shown from Table IX to Table XI in order of increasing the number of SCF calculations required for each molecule. In the estimate requiring three calculations, the results are similar for the three functionals. $\omega$B97X-D gives worse results than other functionals in the estimate requiring two calculations. In the simplest estimate, the HOMO-LUMO gap, which requires only one SCF calculation for each system, $\omega$M05-D significantly outperforms the other two functionals. The reference values of FG115 and detailed HOMO-LUMO gap results by DFT methods are given in the supplementary material [71].

F. Excitation Energies

To assess the performance of density functionals on excitation energies, we perform TDDFT calculations on five small molecules [90], which include nitrogen gas ($N_2$), carbon monoxide (CO), water ($H_2O$), ethylene ($C_2H_4$) and formaldehyde ($CH_2O$), with 6-311(2+,2+)G** basis and EML(99,590) grid. The molecular geometries, experimental values of excitation energy are taken from Ref. [90]. The detail results and mean absolute errors of all excited states are listed in Table XII. The new $\omega$M05-D functional yields excellent performance, especially for the Rydberg
TABLE IX. Statistic errors (in eV) of HOMO-LUMO gaps for the FG115 database. The energy gap of each system is evaluated by only one SCF calculation.

| System   | Error | ωM05-D | M05-2X | ωB97X-D |
|----------|-------|--------|--------|---------|
| atoms    | MSE   | -1.14  | -2.56  | -1.55   |
|          | MAE   | 1.43   | 2.56   | 1.79    |
|          | rms   | 1.62   | 2.79   | 2.05    |
| (18)     | MSE   | -0.62  | -2.00  | -1.15   |
|          | MAE   | 0.73   | 2.00   | 1.15    |
|          | rms   | 0.93   | 2.13   | 1.34    |
| molecules| MSE   | -0.70  | -2.08  | -1.21   |
|          | MAE   | 0.84   | 2.08   | 1.25    |
|          | rms   | 1.07   | 2.24   | 1.48    |
| (97)     | MSE   | -0.95  | -0.83  | -1.04   |
|          | MAE   | 0.98   | 0.87   | 1.08    |
|          | rms   | 1.17   | 1.00   | 1.30    |
| total    | MSE   | -0.70  | -2.08  | -1.21   |
|          | MAE   | 0.84   | 2.08   | 1.25    |
|          | rms   | 1.07   | 2.24   | 1.48    |
| (115)    | MSE   | -0.41  | -0.48  | -0.63   |
|          | MAE   | 0.62   | 0.57   | 0.78    |
|          | rms   | 0.79   | 0.68   | 0.93    |

TABLE X. Statistic errors (in eV) of fundamental gaps for the FG115 database, each evaluated by the difference of HOMO energies between the neutral molecule and anion. The energy gap of each system is evaluated by two SCF calculations.

| System   | Error | ωM05-D | M05-2X | ωB97X-D |
|----------|-------|--------|--------|---------|
| atoms    | MSE   | -0.95  | -0.83  | -1.04   |
|          | MAE   | 0.98   | 0.87   | 1.08    |
|          | rms   | 1.17   | 1.00   | 1.30    |
| (18)     | MSE   | -0.31  | -0.42  | -0.55   |
|          | MAE   | 0.56   | 0.51   | 0.72    |
|          | rms   | 0.70   | 0.60   | 0.85    |
| molecules| MSE   | -0.41  | -0.48  | -0.63   |
|          | MAE   | 0.62   | 0.57   | 0.78    |
|          | rms   | 0.79   | 0.68   | 0.93    |

excitations. Note that ωM05-D outperforms ωB97X-D in both HOMO energies and Rydberg excitations, due to the larger fraction of short-range HF exchange included in ωM05-D (both functionals possess the same amount of LR-HF exchange).

Following Dreuw et al., we perform TDDFT calculations for the lowest charge-transfer (CT) excitation between ethylene and tetrafluoroethylene, with a separation of R. Dreuw et al. have shown that the exact CT excitation
TABLE XI. Statistic errors (in eV) of IP-EA values for the FG115 database. The energy gap of each system is evaluated by three SCF calculations.

| System  | Error | $\omega_{\text{M05-D}}$ | M05-2X | $\omega_{\text{B97X-D}}$ |
|---------|-------|----------------|--------|----------------|----------------|
| atoms   | MSE   | 0.28           | 0.33   | 0.28           |
|         | MAE   | 0.35           | 0.36   | 0.36           |
|         | rms   | 0.60           | 0.63   | 0.59           |
| (18)    | MSE   | 0.34           | 0.42   | 0.22           |
|         | MAE   | 0.44           | 0.50   | 0.39           |
|         | rms   | 0.73           | 0.78   | 0.68           |
| molecules | MSE | 0.33           | 0.40   | 0.23           |
| (97)    | MAE   | 0.43           | 0.48   | 0.39           |
|         | rms   | 0.71           | 0.75   | 0.66           |

energy from the HOMO of donor to the LUMO of acceptor should have the following asymptote [91]:

\[
\omega_{\text{CT}}(R \to \infty) \approx -\frac{1}{R} + \text{IP}_D - \text{EA}_A,
\]  

(48)

where IP$_D$ is the ionization potential of donor and EA$_A$ is the electron affinity of acceptor. Fig. 5 shows the trend of the excitation curves, and indicates the LC hybrid functionals obviously outperforms the global hybrid M05-2X. For the values of the excitation energies, as shown in Fig. 6, $\omega_{\text{M05-D}}$ is about 0.2 electron volt better than $\omega_{\text{B97X-D}}$.

VI. CONCLUSIONS

We have developed a LC hybrid MGGA-D functional, called $\omega_{\text{M05-D}}$, which includes 100% long-range exact exchange, a fraction ($\approx 37\%$) of short-range exact exchange, a modified M05 exchange density functional for short-range interaction, the M05 correlation density functional [18, 19], and empirical atomic-pairwise dispersion corrections. For the modified short-range M05 exchange density functional, we have investigated two models. After comparisons in the training set and test sets, we decide to propose the one based on our new LC scheme $\omega_{\text{M05-D}}$, and marked the trial one as $\omega_{\text{M05s-D}}$. When the constraint of $\omega = 0$ is applied, $\omega_{\text{M05-D}}$ and $\omega_{\text{M05s-D}}$ are both reduced to the existing M05 functional form [18, 19] with the same empirical atomic-pairwise dispersion corrections. The constrained form ($\omega = 0$), when re-optimized on the same training set, provides worse performance on the training set, indicating that the single extra degree of freedom corresponding to long-range exchange is of physical significance to a hybrid MGGA.
TABLE XII. Vertical excitation energies (in eV) of several low-lying excited states of N$_2$, CO, water, formaldehyde and ethylene using 6-311(2+,2+)G** basis set. The geometries and experimental values are taken from Ref. [90].

| Mol. | State | Exp. | $\omega$M05-D | M05-2X | $\omega$B97X-D |
|------|-------|------|---------------|--------|---------------|
|      |       |      |               |        |               |
| $N_2$ | $V^1\Pi_g$ | 9.31 | 9.30 | 9.42 | 9.38 |
|       | $V^1\Sigma_u^+$ | 9.97 | 8.76 | 8.35 | 9.31 |
|       | $V^1\Delta_u$ | 10.27 | 10.14 | 10.51 | 9.82 |
|       | $V^3\Pi_g$ | 7.75 | 7.86 | 8.30 | 7.17 |
|       | $V^3\Delta_u$ | 8.04 | 7.94 | 8.12 | 7.82 |
|       | $V^3\Sigma_u^-$ | 8.88 | 8.74 | 8.35 | 8.23 |
|       | $V^3\Pi_u$ | 9.67 | 8.76 | 9.26 | 9.31 |
|       | $V^3\Pi_u$ | 11.19 | 11.30 | 11.72 | 10.98 |
| $CO$  | $V^1\Pi$ | 8.51 | 8.51 | 8.74 | 8.47 |
|       | $V^1\Sigma^-$ | 9.88 | 9.36 | 9.11 | 9.78 |
|       | $V^3\Pi$ | 6.32 | 6.66 | 7.03 | 6.07 |
|       | $V^3\Sigma^+$ | 8.51 | 8.47 | 8.87 | 8.00 |
|       | $V^3\Delta$ | 9.36 | 9.19 | 9.11 | 8.88 |
|       | $V^3\Sigma^-$ | 9.88 | 9.36 | 9.55 | 9.78 |
| $H_2O$ | $R^1\Pi_1$ | 7.4 | 7.68 | 8.04 | 7.23 |
|       | $R^1\Sigma_1$ | 9.1 | 9.14 | 9.60 | 8.63 |
|       | $R^1\Pi_1$ | 9.7 | 9.73 | 10.29 | 9.20 |
|       | $R^1\Pi_2$ | 10.0 | 9.72 | 10.32 | 9.17 |
|       | $R^1\Pi_2$ | 10.17 | 10.06 | 10.71 | 9.49 |
|       | $R^3\Pi_1$ | 7.2 | 7.27 | 7.66 | 6.89 |
| $C_2H_4$ | $R^1\Pi_{3u}$ | 7.11 | 7.53 | 7.61 | 7.02 |
|       | $V^1\Pi_{1u}$ | 7.60 | 7.80 | 8.07 | 7.52 |
|       | $R^1\Pi_{1g}$ | 7.80 | 7.87 | 8.07 | 7.59 |
|       | $R^1\Pi_{2g}$ | 8.01 | 8.15 | 8.19 | 7.66 |
|       | $R^1\Pi_{2g}$ | 8.29 | 8.36 | 8.52 | 7.87 |
|       | $V^3\Pi_{1u}$ | 8.62 | 8.76 | 8.80 | 8.36 |
|       | $R^3\Pi_{3u}$ | 4.36 | 4.64 | 4.99 | 4.12 |
|       | $R^3\Pi_{3u}$ | 6.98 | 7.43 | 7.48 | 6.92 |
|       | $R^3\Pi_{1g}$ | 7.79 | 7.47 | 7.82 | 7.50 |
|       | $R^3\Pi_{2g}$ | 7.79 | 8.06 | 8.07 | 7.56 |
|       | $R^3\Pi_{2g}$ | 8.15 | 8.12 | 8.11 | 7.63 |
| $CH_2O$ | $V^1\Pi_2$ | 4.07 | 3.63 | 3.68 | 3.88 |
|       | $R^1\Pi_2$ | 7.11 | 7.48 | 7.92 | 6.96 |
|       | $R^1\Pi_2$ | 7.97 | 8.13 | 8.58 | 7.66 |
|       | $R^1\Pi_2$ | 8.14 | 9.13 | 9.47 | 8.74 |
|       | $R^1\Pi_2$ | 8.37 | 8.30 | 8.84 | 7.84 |
|       | $R^1\Pi_2$ | 8.88 | 8.86 | 9.21 | 8.52 |
|       | $V^3\Pi_2$ | 3.50 | 3.02 | 3.12 | 3.21 |
|       | $V^3\Pi_1$ | 5.86 | 5.70 | 6.02 | 5.29 |
|       | $R^3\Pi_2$ | 6.83 | 7.33 | 7.74 | 6.81 |
|       | $R^3\Pi_2$ | 7.79 | 7.97 | 8.37 | 7.50 |
|       | $R^3\Pi_2$ | 7.96 | 8.06 | 8.45 | 7.56 |
|      | MAE Valence | 0.31 | 0.46 | 0.32 |
|      | MAE Rydberg | 0.22 | 0.47 | 0.35 |
FIG. 5. The lowest CT excitation of \( \text{C}_2\text{H}_4 \cdots \text{C}_2\text{F}_4 \) dimer along the intermolecular distance \( R \) (in Å). For all functionals, the excitation at 5 Å is set to zero.

Since \( \omega \text{M05-D} \) is a parametrized functional, we test it against the trial simple model \( \omega \text{M05s-D} \) as well as two closely related functionals (M05-2X [19] and \( \omega \text{B97X-D} \) [36]) on a separate independent test set of data, which includes further atomization energies, reaction energies, noncovalent interaction energies, equilibrium geometries, energy curve for homonuclear diatomic cation dissociations, frontier orbital energies and fundamental gaps. The three databases assessing frontier orbital energies and fundamental gaps are presented for the first time. For excitation energies, we calculate valence and Rydberg excitations, as well as a charge-transfer excited state. Compared to \( \omega \text{M05s-D} \), noticeable difference in transferability for atomization energies largely decides our proposed model. \( \omega \text{M05-D} \) consistently outperforms M05-2X (and performs comparably to \( \omega \text{B97X-D} \)) on the test sets, and shows smaller SIE and better asymptotic behavior relative to both the M05-2X and \( \omega \text{B97X-D} \).
FIG. 6. The lowest CT excitation of $\text{C}_2\text{H}_4\cdots\text{C}_2\text{F}_4$ dimer along the intermolecular distance $R$ (in Å).

ACKNOWLEDGMENTS

This work was supported by National Science Council of Taiwan (Grant No. NSC98-2112-M-002-023-MY3), National Taiwan University (Grant No. 99R70304 and 10R80914-1), and NCTS of Taiwan.

[1] P. Hohenberg and W. Kohn, Phys. Rev. 136, B864 (1964).
[2] W. Kohn and L. J. Sham, Phys. Rev. 140, A1133 (1965).
[3] R. G. Parr and W. Yang, Density-Functional Theory of Atoms and Molecules (Oxford University Press, New York, 1989).
[4] R. M. Dreizler and E. K. U. Gross, Density Functional Theory: An Approach to the Quantum Many Body Problem (Springer-Verlag, Berlin, 1990).
[5] E. Engel and R. M. Dreizler, Density Functional Theory: An Advanced Course (Springer-Verlag, Berlin, 2011).
[6] W. Kohn, A. D. Becke, and R. G. Parr, J. Phys. Chem. 100, 12974 (1996).
[7] M. E. Casida, Recent Advances in Density Functional Methods, Part I (World Scientific, Singapore, 1995).
[8] E. K. U. Gross, J. F. Dobson, and M. Petersilka, *Density Functional Theory II* (Springer, Heidelberg, 1996).

[9] T. V. Voorhis and G. E. Scuseria, J. Chem. Phys. 109, 400 (1998).

[10] J. Tao, J. P. Perdew, V. N. Staroverov, and G. E. Scuseria, Phys. Rev. Lett. 91, 146401 (2003).

[11] Y. Zhao and D. G. Truhlar, J. Chem. Phys. 125, 194101 (2006).

[12] A. D. Becke, J. Chem. Phys. 104, 1040 (1996).

[13] A. D. Boese and N. C. Handy, J. Chem. Phys. 116, 9559 (2002).

[14] V. N. Staroverov, G. E. Scuseria, J. Tao, and J. P. Perdew, J. Chem. Phys. 119, 12129 (2003).

[15] Y. Zhao, B. J. Lynch, and D. G. Truhlar, J. Phys. Chem. A 108, 2715 (2004).

[16] J. G. Hill, J. A. Platts, and H.-J. Werner, Phys. Chem. Chem. Phys. 8, 4072 (2006).

[17] A. D. Boese and J. M. L. Martin, J. Chem. Phys. 121, 3405 (2004).

[18] Y. Zhao, N. E. Schultz, and D. G. Truhlar, J. Chem. Phys. 123, 161103 (2005).

[19] Y. Zhao, N. E. Schultz, and D. G. Truhlar, J. Chem. Theory Comput. 2, 364 (2006).

[20] Y. Zhao and D. G. Truhlar, Theor. Chem. Acc. 120, 215 (2008).

[21] A. D. Becke, Int. J. Quantum Chem. 23, 1915 (1983).

[22] A. D. Becke, J. Chem. Phys. 109, 2092 (1998).

[23] A. D. Becke, J. Chem. Phys. 112, 4020 (2000).

[24] H. L. Schmider and A. D. Becke, THEOCHEM 527, 51 (2000).

[25] Y. Zhao and D. G. Truhlar, Acc. Chem. Res. 41, 157 (2008).

[26] Y. Zhao and D. G. Truhlar, J. Chem. Theory Comput. 4, 1849 (2008).

[27] H. Iikura, T. Tsuneda, T. Yanai, and K. Hirao, J. Chem. Phys. 115, 3540 (2001).

[28] Y. Tawada, T. Tsuneda, S. Yanagisawa, T. Yanai, and K. Hirao, J. Chem. Phys. 120, 8425 (2004).

[29] I. C. Gerber and J. G. Ángyán, Chem. Phys. Lett. 415, 100 (2005).

[30] I. C. Gerber, J. G. Ángyán, M. Marsman, and G. Kresse, J. Chem. Phys. 127, 054101 (2007).

[31] O. A. Vydrov, J. Heyd, A. V. Krukau, and G. E. Scuseria, J. Chem. Phys. 125, 074106 (2006).

[32] O. A. Vydrov and G. E. Scuseria, J. Chem. Phys. 125, 234109 (2006).

[33] J.-W. Song, T. Hirosawa, T. Tsuneda, and K. Hirao, J. Chem. Phys. 126, 154105 (2007).

[34] A. J. Cohen, P. Mori-Sánchez, and W. Yang, J. Chem. Phys. 126, 191109 (2007).

[35] J.-D. Chai and M. Head-Gordon, J. Chem. Phys. 128, 084106 (2008).

[36] J.-D. Chai and M. Head-Gordon, Phys. Chem. Chem. Phys. 10, 6615 (2008).

[37] J.-D. Chai and M. Head-Gordon, J. Chem. Phys. 131, 174105 (2009).

[38] A. D. Becke, J. Chem. Phys. 98, 5648 (1993).
[39] P. J. Stephens, F. J. Devlin, C. F. Chabalowski, and M. J. Frisch, J. Phys. Chem. 98, 11623 (1994).
[40] A. D. Becke, J. Chem. Phys. 107, 8554 (1997).
[41] J. F. Dobson, K. McLennan, A. Rubio, J. Wang, T. Gould, H. M. Le, and B. P. Dinte, Aust. J. Chem. 54, 513 (2001).
[42] S. Kristyan and P. Pulay, Chem. Phys. Lett. 229, 175 (1994).
[43] X. Wu, M. C. Vargas, S. Nayak, V. Lotrich, and G. Scoles, J. Chem. Phys. 115, 8748 (2001); Q. Wu and W. Yang, ibid. 116, 515 (2002); U. Zimmerli, M. Parrinello, and P. Koumoutsakos, ibid. 120, 2693 (2004); S. Grimme, J. Comput. Chem. 25, 1463 (2004); 27, 1787 (2006); J. Antony and S. Grimme, Phys. Chem. Chem. Phys. 8, 5287 (2006); P. Jurečka, J. Černý, P. Hobza, and D. R. Salahub, J. Comput. Chem. 28, 555 (2006); A. Goursot, T. Mineva, R. Kevorkyants, and D. Talbi, J. Chem. Theory Comput. 3, 755 (2007); S. Grimme, J. Antony, T. Schwabe, and C. Mück-Lichtenfeld, Org. Biomol. Chem. 5, 741 (2007); J. Černý, P. Jurečka, P. Hobza, and H. Valdés, J. Phys. Chem. A 111, 1146 (2007); C. Morgado, M. A. Vincent, I. H. Hillier, and X. Shan, Phys. Chem. Chem. Phys. 9, 448 (2007); M. Kabeláč, H. Valdés, E. C. Sherer, C. J. Cramer, and P. Hobza, 9, 5000 (2007); P. Jurečka and P. Hobza, 9, 5291 (2007).
[44] S. Grimme, J. Chem. Phys. 124, 034108 (2006).
[45] T. Schwabe and S. Grimme, Phys. Chem. Chem. Phys. 9, 3397 (2007).
[46] A. Tarnopolsky, A. Karton, R. Sertchook, D. Vuzman, and J. M. L. Martin, J. Phys. Chem. A 112, 3 (2008).
[47] T. Benighaus, R. A. DiStasio, Jr., R. C. Lochan, J.-D. Chai, and M. Head-Gordon, J. Phys. Chem. A 112, 2702 (2008).
[48] Y. Zhang, X. Xu, and W. A. Goddard, III, Proc. Natl. Acad. Sci. U.S.A. 106, 4963 (2009).
[49] R. Peverati and D. G. Truhlar, J. Phys. Chem. Lett. 2, 2810 (2011).
[50] P. M. W. Gill, R. D. Adamson, and J. A. Pople, Mol. Phys. 88, 1005 (1996).
[51] T. M. Henderson, B. G. Janesko, and G. E. Scuseria, J. Chem. Phys. 128, 194105 (2008).
[52] M. Ernzerhof and J. P. Perdew, J. Chem. Phys. 109, 3313 (1998).
[53] J. P. Perdew, K. Burke, and M. Ernzerhof, Phys. Rev. Lett. 77, 3865 (1996); 78, 1396(E) (1997).
[54] L. A. Constantin, J. P. Perdew, and J. Tao, Phys. Rev. B 73, 205104 (2006).
[55] von Weizsäcker, C. F. Z. Phys. 96, 431 (1935).
[56] J. P. Perdew and Y. Wang, Phys. Rev. B 45, 13244 (1992).
[57] H. Stoll, C. M. E. Pavlidou, and H. Preuss, Theor. Chim. Acta 49, 143 (1978); H. Stoll, E. Golka, and H. Preuss, 55, 29 (1980).
[58] S. J. Chakravorty, S. R. Gwaltney, E. R. Davidson, F. A. Parpia, and C. F. Fischer, Phys. Rev. A 47, 3649 (1993).
[59] L. A. Curtiss, K. Raghavachari, P. C. Redfern, and J. A. Pople, J. Chem. Phys. 106, 1063 (1997).
[60] L. A. Curtiss, P. C. Redfern, K. Raghavachari, and J. A. Pople, J. Chem. Phys. 109, 42 (1998).
[61] L. A. Curtiss, K. Raghavachari, P. C. Redfern, and J. A. Pople, J. Chem. Phys. 112, 7374 (2000).
[62] J. A. Pople, M. Head-Gordon, D. J. Fox, K. Raghavachari, and L. A. Curtiss, J. Chem. Phys. 90, 5622 (1989).
[63] Y. Zhao, N. González-García, and D. G. Truhlar, J. Phys. Chem. A 109, 2012 (2005); 110, 4942(E) (2006).
[64] P. Jurečka, J. Šponer, J. Černý, and P. Hobza, Phys. Chem. Chem. Phys. 8, 1985 (2006).
[65] S. E. Wheeler and K. N. Houk, J. Chem. Theory Comput. 6, 395 (2010).
[66] Y. Shao, L. Fusti-Molnar, Y. Jung, J. Kussmann, C. Ochsenfeld, S. T. Brown, A. T. B. Gilbert, L. V. Slipchenko, S. V. Levchenko, D. P. O’Neill, R. A. DiStasio, Jr., R. C. Lochan, T. Wang, G. J. O. Beran, N. A. Besley, J. M. Herbert, C. Y. Lin, T. V. Voorhis, S. H. Chien, A. Sodt, R. P. Steele, V. A. Rassolov, P. E. Maslen, P. P. Korambath, R. D. Adamson, B. Austin, J. Baker, E. F. C. Byrd, H. Dachsel, R. J. Doerksen, A. Dreuw, B. D. Dunietz, A. D. Dutoi, T. R. Furlani, S. R. Gwaltney, A. Heyden, S. Hirata, C.-P. Hsu, G. Kedziora, R. Z. Khallilulin, P. Klunzinger, A. M. Lee, M. S. Lee, W. Liang, I. Lotan, N. Nair, B. Peters, E. I. Proynov, P. A. Pieniazek, Y. M. Rhee, J. Ritchie, E. Rosta, C. D. Sherrill, A. C. Simmonett, J. E. Subotnik, H. L. Woodcock, III, W. Zhang, A. T. Bell, A. K. Chakraborty, D. M. Chipman, F. J. Keil, A. Warshel, W. J. Hehre, H. F. Schaefer, III, J. Kong, A. I. Krylov, P. M. W. Gill, and M. Head-Gordon, Phys. Chem. Chem. Phys. 8, 3172 (2006).
[67] S. F. Boys and F. Bernardi, Mol. Phys. 19, 553 (1970).
[68] C. W. Murray, N. C. Handy, and G. J. Laming, Mol. Phys. 78, 997 (1993).
[69] V. I. Lebedev, Zh. Vychisl. Mat. Mat. Fiz. 15, 48 (1975); 16, 293 (1976); Sibirsk. Mat. Zh. 18, 132 (1977).
[70] M. S. Marshall, L. A. Burns, and C. D. Sherrill, J. Chem. Phys. 135, 194102 (2011).
[71] See supplementary material at [URL will be inserted by AIP] for the reference values and molecular geometries of the IP131, EA115 and FG115 databases, as well as some detailed DFT results.
[72] L. A. Curtiss, P. C. Redfern, and K. Raghavachari, J. Chem. Phys. 123, 124107 (2005).
[73] R. A. DiStasio, Jr., R. P. Steele, Y. M. Rhee, Y. Shao, and M. Head-Gordon, J. Comput. Chem. 28, 839 (2007).
[74] T. Bally and G. N. Sastry, J. Phys. Chem. A 101, 7923 (1997); B. Braïda, P. C. Hiberty, and A. Savin, 102, 7872 (1998); P. Mori-Sánchez, A. J. Cohen, and W. Yang, J. Chem. Phys. 125, 201102 (2006); A. Ruzsinszky, J. P. Perdew, G. I. Csonka, O. A. Vydzov, and G. E. Scuseria, 126, 104102 (2007).
[75] A. D. Dutoi and M. Head-Gordon, Chem. Phys. Lett. 422, 230 (2006).
[76] J. Gräfenstein, E. Kraka, and D. Cremer, J. Chem. Phys. 120(2), 524 (2004).
[77] J. Gräfenstein, E. Kraka, and D. Cremer, Phys. Chem. Chem. Phys. 6, 1096 (2004).
[78] J. P. Perdew and A. Zunger, Phys. Rev. B 23, 5048 (1981).
[79] G. D. Purvis and R. J. Bartlett, J. Chem. Phys. 76, 1910 (1982).
[80] K. Raghavachari, G. W. Trucks, J. A. Pople, and M. Head-Gordon, Chem. Phys. Lett. 157, 479 (1989).
[81] M. Levy, J. P. Perdew, and V. Sahni, Phys. Rev. A 30, 2745 (1984).
[82] L. J. Sham and M. Schlüter, Phys. Rev. Lett. 51, 1888 (1983).
[83] L. J. Sham and M. Schlüter, Phys. Rev. B 32, 3883 (1985).
[84] J. P. Perdew and M. Levy, Phys. Rev. Lett. 51 (1983).
[85] T. Tsuneda, J.-W. Song, S. Suzuki, and K. Hirao, J. Chem. Phys. 133, 174101 (2010).
[86] NIST Computational Chemistry Comparison and Benchmark Database, NIST Standard Reference Database Number 101, Release 15b, August 2011, Editor: Russell D. Johnson III, [http://cccbdb.nist.gov/]
[87] P. M. W. Gill, B. G. Johnson, J. A. Pople, and M. J. Frisch, Int. J. Quantum Chem. Symp. 26, 319 (1992); C. R. Brundle, M. B. Robin, N. A. Kuebler, and H. J. Basch, J. Am. Chem. Soc. 94, 1451 (1972); W. von Niessen, L. Åsbrink, and G. Bieri, J. Electron Spectrosc. Relat. Phenom. 26, 173 (1982); E. A. Colbourne, J. M. Dyke, E. P. F. Lee, A. Morris, and I. R. Trickle, Mol. Phys. 35, 873 (1978); D. C. Frost, S. T. Lee, and C. A. McDowell, Chem. Phys. Lett. 17, 153 (1972); G. Bieri, L. Åsbrink, and W. von Niessen, J. Electron Spectrosc. Relat. Phenom. 27, 129 (1982); T. Cvitas, H. Güsten, L. Klasinc, I. Novak, and H. Vansik, Z. Naturforsch. A 32A, 1528 (1977); G. Bieri, L. Åsbrink, and W. von Niessen, J. Electron Spectrosc. Relat. Phenom. 23, 281 (1981); L. Åsbrink, W. von Niessen, and G. Bieri, 21, 93 (1980); U. Gelius, C. J. Allan, D. A. Allison, H. Siegbahn, and K. Siegbahn, Chem. Phys. Lett. 11, 224 (1971); L. Åsbrink, A. Svensson, W. von Niessen, and G. Bieri, J. Electron Spectrosc. Relat. Phenom. 24, 293 (1981); G. Bieri and L. Åsbrink, 20, 149 (1980); W. von Niessen, G. Bieri, and L. Åsbrink, 21, 175 (1980).
[88] A. Halkier, T. Helgaker, P. Jørgensen, W. Klopper, H. Koch, J. Olsen, and A. K. Wilson, Chem. Phys. Lett. 286, 243 (1998).
[89] J. F. Janak, Phys. Rev. B 18, 7165 (1978).
[90] S. Hirata and M. Head-Gordon, Chem. Phys. Lett. 314, 291 (1999).
[91] A. Drea, J. L. Weisman, and M. Head-Gordon, J. Chem. Phys. 119, 2943 (2003).
[92] Y. Zhao and D. G. Truhlar, J. Phys. Chem. A 109, 5656 (2005).
SUPPLEMENTARY MATERIAL

TABLE XIII: \(-\epsilon_N(N)\) (in eV) of IP131 database. Most experimental reference values are collected from the NIST database, while other publications are adopted for the molecules marked.

| Molecule                  | Reference | \(\omega\)M05-D | M05-2X | \(\omega\)B97X-D |
|---------------------------|-----------|-----------------|--------|------------------|
| H (Hydrogen atom)         | 13.60     | 11.10           | 10.44  | 11.04            |
| He (Helium atom)          | 24.59     | 20.75           | 20.75  | 20.18            |
| Li (Lithium atom)         | 5.39      | 5.06            | 4.19   | 5.22             |
| Be (Beryllium atom) [87]  | 9.32      | 8.19            | 7.29   | 8.27             |
| B (Boron atom)            | 8.30      | 7.21            | 6.39   | 7.24             |
| C (Carbon atom)           | 11.26     | 9.74            | 9.11   | 9.57             |
| N (Nitrogen atom)         | 14.53     | 12.46           | 12.02  | 12.13            |
| O (Oxygen atom)           | 13.62     | 11.80           | 11.51  | 11.48            |
| F (Fluorine atom)         | 17.42     | 15.15           | 15.10  | 14.63            |
| Ne (Neon atom)            | 21.57     | 18.77           | 18.93  | 18.06            |
| Na (Sodium atom)          | 5.14      | 4.92            | 4.08   | 4.87             |
| Mg (Magnesium atom)       | 7.65      | 7.15            | 6.36   | 7.07             |
| Al (Aluminum atom)        | 5.99      | 5.33            | 4.43   | 5.47             |
| Si (Silicon atom)         | 8.15      | 7.29            | 6.42   | 7.29             |
| P (Phosphorus atom)       | 10.49     | 9.33            | 8.51   | 9.25             |
| S (Sulfur atom)           | 10.36     | 9.33            | 8.65   | 9.30             |
| Cl (Chlorine atom)        | 12.97     | 11.70           | 11.12  | 11.56            |
| Ar (Argon atom)           | 15.76     | 14.17           | 13.68  | 13.93            |
| CH\(_3\) (Methyl radical) | 9.84      | 8.79            | 7.92   | 8.60             |
| CH\(_4\) (Methane)        | 13.60     | 13.16           | 12.59  | 12.97            |
| NH (Imidogen) (\(^3\Sigma^-\)) | 13.49   | 11.97           | 11.51  | 11.64            |
| NH\(_2\) (Amino radical)  | 12.00     | 10.99           | 10.47  | 10.74            |
| NH\(_3\) (Ammonia)        | 10.82     | 10.01           | 9.41   | 9.74             |
| OH (Hydroxyl radical)     | 13.02     | 11.64           | 11.32  | 11.26            |
| Molecular Formula | Property 1 | Property 2 | Property 3 | Property 4 |
|-------------------|------------|------------|------------|------------|
| H₂O (Water)       | 12.62      | 11.51      | 11.10      | 11.10      |
| HF (Hydrogen fluoride) | 16.12     | 14.42      | 14.28      | 13.90      |
| SiH₃ (Silyl)      | 8.74       | 8.19       | 7.32       | 8.16       |
| SiH₄ (Silane)     | 12.30      | 11.86      | 11.18      | 11.80      |
| PH₃ (Phosphine)   | 10.59      | 9.79       | 9.03       | 9.76       |
| H₂S (Hydrogen sulfide) | 10.50    | 9.57       | 8.84       | 9.47       |
| HCl (Hydrogen sulfide) | 12.77     | 11.64      | 11.02      | 11.45      |
| C₂H₂ (Acetylene)  | 11.49      | 10.61      | 9.85       | 10.36      |
| C₂H₄ (Ethylene)   | 10.68      | 10.01      | 9.17       | 9.74       |
| C₂H₆ (Ethane)     | 11.99      | 11.70      | 11.15      | 11.59      |
| HCN (Hydrogen cyanide) | 13.61     | 12.62      | 11.97      | 12.35      |
| CO (Carbon monoxide) | 14.01     | 12.97      | 12.51      | 12.81      |
| HCO (Formyl radical) | 9.31      | 8.81       | 8.30       | 8.62       |
| H₂CO (Formaldehyde) | 10.89     | 10.09      | 9.60       | 9.82       |
| CH₃OH (Methyl alcohol) | 10.96     | 10.23      | 9.76       | 9.93       |
| N₂ (Nitrogen diatomic) | 15.58     | 14.58      | 14.25      | 14.28      |
| N₂H₄ (Hydrazine)  | 8.98       | 9.03       | 8.46       | 8.79       |
| NO (Nitric oxide) | 9.26       | 8.70       | 8.35       | 8.35       |
| O₂ (Oxygen diatomic) (³Σ_g) | 12.30     | 11.48      | 11.26      | 11.02      |
| H₂O₂ (Hydrogen peroxide) | 11.70    | 10.77      | 10.42      | 10.36      |
| F₂ (Fluorine diatomic) | 15.70     | 14.44      | 14.39      | 13.90      |
| CO₂ (Carbon dioxide) | 13.78     | 12.97      | 12.54      | 12.65      |
| P₂ (Phosphorus diatomic) | 10.62     | 9.93       | 9.14       | 9.90       |
| S₂ (Sulfur diatomic) (³Σ_g) | 9.55      | 8.95       | 8.30       | 8.87       |
| Cl₂ (Chlorine diatomic) | 11.49     | 10.77      | 10.17      | 10.64      |
| NaCl (Sodium Chloride) | 9.80      | 8.60       | 7.94       | 8.40       |
| SiO (Silicon monoxide) [87] | 11.61     | 10.88      | 10.20      | 10.77      |
| CS (Carbon monosulfide) [87] | 11.34     | 10.99      | 10.42      | 10.91      |
| ClO (Monochlorine monoxide) | 11.01     | 10.12      | 9.71       | 9.90       |
| ClF (Chlorine monofluoride) | 12.77     | 11.67      | 11.18      | 11.45      |
| Si₂H₆ (Disilane)  | 10.53      | 10.15      | 9.41       | 10.12      |
| Molecular Formula   | 34°C   | 38°C   | 42°C   | 46°C   |
|---------------------|--------|--------|--------|--------|
| CH₃Cl (Methyl chloride) | 11.29  | 10.61  | 9.98   | 10.42  |
| CH₃SH (Methanethiol) | 9.44   | 8.79   | 8.05   | 8.68   |
| SO₂ (Sulfur dioxide) | 12.50  | 11.78  | 11.29  | 11.59  |
| BF₃ (Borane, trifluoro-) | 15.96  | 14.82  | 14.72  | 14.28  |
| BCl₃ (Borane, trichloro-) | 11.64  | 11.18  | 10.58  | 11.02  |
| AlCl₃ (Aluminum trichloride) | 12.01  | 11.48  | 10.85  | 11.29  |
| CF₄ (Carbon tetrafluoride) | 16.20  | 15.23  | 15.15  | 14.69  |
| CCl₄ (Carbon tetrachloride) | 11.69  | 11.15  | 10.58  | 10.99  |
| OCS (Carbonyl sulfide) | 11.19  | 10.64  | 9.96   | 10.53  |
| CS₂ (Carbon disulfide) | 10.09  | 9.57   | 8.89   | 9.57   |
| CF₂O (Carbonic difluoride) | 13.60  | 12.78  | 12.43  | 12.38  |
| SiF₄ (Silicon tetrafluoride) | 16.40  | 15.37  | 15.26  | 14.85  |
| N₂O (Nitrous oxide) | 12.89  | 12.00  | 11.51  | 11.75  |
| NF₃ (Nitrogen trifluoride) | 13.60  | 12.62  | 12.35  | 12.32  |
| PF₃ (Phosphorus trifluoride) | 12.20  | 10.74  | 10.17  | 10.69  |
| O₃ (Ozone) | 12.73  | 12.35  | 11.91  | 11.97  |
| F₂O (Difluorine monoxide) | 13.26  | 12.51  | 12.40  | 12.02  |
| CIF₃ (Chlorine trifluoride) | 13.05  | 12.19  | 11.86  | 11.86  |
| C₂F₄ (Tetrafluoroethylene) | 10.69  | 9.93   | 9.41   | 9.71   |
| CF₃CN (Acetonitrile, trifluoro-) | 14.30  | 13.30  | 12.73  | 13.00  |
| CH₃CCH (Propyne) | 10.37  | 9.82   | 9.08   | 9.60   |
| CH₂CCH₂ (Allene) | 10.20  | 9.79   | 9.06   | 9.60   |
| C₃H₄ (Cyclopropene) | 9.86   | 9.33   | 8.60   | 9.11   |
| C₃H₆ (Cyclopropane) | 10.54  | 10.47  | 9.74   | 10.28  |
| C₃H₈ (Propane) | 11.51  | 11.21  | 10.66  | 11.10  |
| CH₃CCCH₃ (2-Butyne) | 9.79   | 9.19   | 8.46   | 8.98   |
| C₄H₆ (Cyclobutene) | 9.43   | 9.19   | 8.43   | 8.98   |
| CH₃CH(CH₃)CH₃ (Isobutane) | 11.13  | 10.99  | 10.42  | 10.85  |
| C₆H₆ (Benzene) | 9.25   | 9.28   | 8.49   | 9.06   |
| CH₂F₂ (Methane, difluoro-) | 13.27  | 12.27  | 11.97  | 11.97  |
| CHF₃ (Methane, trifluoro-) | 15.50  | 13.52  | 13.27  | 13.22  |
| Compound                                | A | B | C | D |
|-----------------------------------------|---|---|---|---|
| CH₂Cl₂ (Methylene chloride)             | 11.40 | 10.85 | 10.28 | 10.72 |
| CHCl₃ (Chloroform)                      | 11.50 | 10.85 | 10.28 | 10.72 |
| CH₃NO₂ (Methane, nitro-)                | 11.29 | 11.12 | 10.77 | 10.72 |
| CH₃SiH₃ (Methyl silane)                 | 11.60 | 11.23 | 10.50 | 11.12 |
| HCOOH (Formic acid)                     | 11.50 | 10.69 | 10.23 | 10.36 |
| CH₃CONH₂ (Acetamide)                    | 10.00 | 9.66  | 9.17  | 9.36  |
| C₂H₅N (Aziridine)                       | 9.85  | 9.36  | 8.73  | 9.11  |
| C₂N₂ (Cyanogen)                         | 13.51 | 12.78 | 12.19 | 12.54 |
| CH₃NHCH₃ (Dimethylamine)                | 8.95  | 8.60  | 7.97  | 8.38  |
| CH₂CO (Ketene)                          | 9.64  | 9.19  | 8.49  | 9.00  |
| C₂H₄O (Ethylene oxide)                  | 10.57 | 10.25 | 9.79  | 9.90  |
| C₂H₂O₂ (Ethanedial)                     | 10.60 | 10.12 | 9.63  | 9.87  |
| CH₃CH₂OH (Ethanol)                      | 10.64 | 10.09 | 9.63  | 9.79  |
| CH₃OCH₃ (Dimethyl ether)                | 10.10 | 9.66  | 9.14  | 9.36  |
| C₂H₄S (Thiirane)                        | 9.05  | 8.57  | 7.86  | 8.46  |
| CH₃SOCH₃ (Dimethyl sulfoxide)           | 9.10  | 8.76  | 8.16  | 8.57  |
| CH₂CHF (Ethene, fluoro-)                | 10.63 | 9.90  | 9.17  | 9.66  |
| CH₃CH₂Cl (Ethyl chloride)               | 11.06 | 10.44 | 9.85  | 10.28 |
| CH₂CHCl (Ethene, chloro-)               | 10.20 | 9.60  | 8.87  | 9.41  |
| CH₃COCl (Acetyl Chloride)               | 11.03 | 10.77 | 10.23 | 10.53 |
| CH₂ClCH₂CH₃ (Propane, 1-chloro-)        | 10.88 | 10.42 | 9.76  | 10.25 |
| N(CH₃)₃ (Trimethylamine)                | 8.54  | 8.27  | 7.62  | 8.05  |
| C₄H₄O (Furan)                           | 8.90  | 8.70  | 7.92  | 8.51  |
| C₄H₅N (Pyrrole)                         | 8.23  | 8.13  | 7.32  | 7.92  |
| NO₂ (Nitrogen dioxide)                  | 11.23 | 10.72 | 10.42 | 10.36 |
| SF₆ (Sulfur Hexafluoride) [87]           | 15.70 | 14.96 | 14.91 | 14.42 |
| CFCl₃ (Trichloromonofluoromethane)      | 11.76 | 11.23 | 10.66 | 11.07 |
| CF₃Cl (Methane, chlorotrifluoro-)       | 13.08 | 12.27 | 11.75 | 12.05 |
| CF₃Br (Bromotrifluoromethane) [87]      | 12.08 | 11.29 | 10.74 | 11.12 |
| HCCF (Fluoroacetylene) [87]             | 11.50 | 10.53 | 9.85  | 10.28 |
| HCCCCN (Cyanoacetylene) [87]            | 11.75 | 11.07 | 10.42 | 10.85 |
| molecule                              | $-\epsilon_{N+1}(N + 1)$ | $-\epsilon_{N+1}(N)$ | $-\epsilon_{N+1}(N + 1)$ | $-\epsilon_{N+1}(N)$ | $-\epsilon_{N+1}(N + 1)$ | $-\epsilon_{N+1}(N)$ |
|--------------------------------------|--------------------|---------------------|------------------------|---------------------|------------------------|---------------------|
| C$_4$N$_2$ (2-Butynedinitrile)       | 11.84              | 11.56               | 10.96                  | 11.34               |
| C$_2$N$_2$ (Cyanogen)                | 13.51              | 12.78               | 12.19                  | 12.54               |
| C$_3$O$_2$ (Carbon suboxide)         | 10.80              | 10.39               | 9.82                   | 10.23               |
| FCN (Cyanogen fluoride)              | 13.65              | 12.46               | 11.89                  | 12.16               |
| C$_4$H$_2$ (Diacetylene)             | 10.30              | 9.71                | 9.00                   | 9.52                |
| H$_2$CS (Thioformaldehyde)           | 9.38               | 8.73                | 8.02                   | 8.62                |
| CHONH$_2$ (Formamide)                | 10.40              | 9.90                | 9.44                   | 9.57                |
| CH$_2$CHCHO (Acrolein)              | 10.10              | 9.90                | 9.38                   | 9.57                |
| CH$_2$CCl$_2$ (Ethene, 1,1-dichloro-) | 10.00          | 9.57                | 8.87                   | 9.41                |
| C$_2$HF$_3$ (Trifluoroethylene)      | 10.62              | 9.74                | 9.14                   | 9.52                |
| CH$_2$CF$_2$ (Ethene, 1,1-difluoro-) | 10.70              | 10.01               | 9.33                   | 9.76                |
| CH$_3$F (Methyl fluoride)            | 13.04              | 12.21               | 11.86                  | 11.91               |
| CF$_2$Cl$_2$ (Difluorodichloromethane)| 12.24            | 11.61               | 11.07                  | 11.45               |
| SiF$_2$ (Silicon difluoride)         | 11.08              | 10.25               | 9.52                   | 10.23               |
| MSE                                  | -0.79              | -1.34               | -1.02                  |                     |
| MAE                                  | 0.79               | 1.34                | 1.02                   |                     |
| rms                                  | 0.96               | 1.43                | 1.18                   |                     |

TABLE XIV: $-\epsilon_{N+1}(N + 1)$ and $-\epsilon_{N+1}(N)$ (in eV) of EA115 database. Reference values are calculated by the CCSD(T) theory.
| Substance                        | X  | Y  | Z  | X' | Y' | Z' | X'' | Y'' | Z'' |
|---------------------------------|----|----|----|----|----|----|-----|-----|-----|
| F (Fluorine atom)               | 3.44 | 2.28 | 4.30 | 1.90 | 4.81 | 1.93 | 4.90 |
| Ne (Neon atom)                  | -5.31 | -7.18 | -7.07 | -8.16 | -5.82 | -7.53 | -6.83 |
| Na (Sodium atom)                | 0.54 | 0.68 | -0.49 | 0.05 | -0.03 | 0.68 | -0.24 |
| Mg (Magnesium atom)             | -0.23 | -0.41 | -0.65 | -0.98 | 0.11 | -0.30 | -0.38 |
| Al (Aluminum atom)              | 0.45 | 0.27 | 0.22 | -0.54 | 1.12 | 0.33 | 0.35 |
| Si (Silicon atom)               | 1.42 | 1.09 | 1.41 | 0.22 | 2.31 | 1.06 | 1.55 |
| P (Phosphorus atom)             | 0.74 | 0.57 | 0.98 | -0.24 | 2.20 | 0.63 | 1.20 |
| S (Sulfur atom)                 | 2.10 | 1.77 | 2.53 | 1.01 | 3.64 | 1.71 | 2.77 |
| Cl (Chlorine atom)              | 3.69 | 3.05 | 4.27 | 2.34 | 5.22 | 2.91 | 4.57 |
| Ar (Argon atom)                 | -2.81 | -3.18 | -3.78 | -4.03 | -2.53 | -3.48 | -3.40 |
| CH₃ (Methyl radical)            | -0.07 | -0.08 | -0.08 | -0.92 | 1.09 | -0.16 | -0.05 |
| CH₄ (Methane)                   | -0.62 | -1.01 | -1.52 | -1.58 | -0.92 | -0.92 | -1.17 |
| NH (Imidogen)                   | 0.33 | -0.03 | 0.65 | -0.79 | 1.66 | -0.14 | 0.84 |
| NH₂ (Amino radical)             | 0.74 | 0.44 | 0.90 | -0.33 | 1.85 | 0.27 | 1.12 |
| NH₃ (Ammonia)                   | -0.56 | -0.98 | -1.52 | -1.63 | -0.76 | -0.90 | -1.12 |
| OH (Hydroxyl radical)           | 1.83 | 1.22 | 2.15 | 0.63 | 2.91 | 0.95 | 2.53 |
| H₂O (Water)                     | -0.56 | -1.03 | -1.50 | -1.80 | -0.68 | -0.95 | -1.09 |
| HF (Hydrogen fluoride)          | -0.63 | -1.14 | -1.47 | -1.85 | -0.73 | -1.01 | -1.12 |
| SiH₃ (Silyl)                    | 0.93 | 0.79 | 1.14 | -0.03 | 2.53 | 0.82 | 1.31 |
| SiH₄ (Silane)                   | -1.11 | -1.09 | -1.69 | -1.60 | -0.95 | -1.06 | -1.28 |
| PH₃ (Phosphine)                 | -1.21 | -0.90 | -1.50 | -1.44 | -0.71 | -0.90 | -1.09 |
| SH₂ (Hydrogen sulfide)          | -0.49 | -1.85 | -1.41 | -2.39 | -0.63 | -1.69 | -1.03 |
| HCl (Hydrogen chloride)         | -0.52 | -0.92 | -1.36 | -1.63 | -0.54 | -0.84 | -0.98 |
| C₂H₂ (Acetylene)                | -1.90 | -2.50 | -1.52 | -3.24 | -1.09 | -2.56 | -1.22 |
| C₂H₄ (Ethylene)                 | -1.86 | -2.07 | -1.74 | -2.86 | -0.92 | -2.12 | -1.33 |
| C₂H₆ (Ethane)                   | -0.62 | -1.03 | -1.55 | -1.55 | -0.90 | -0.95 | -1.17 |
| HCN (Hydrogen cyanide)          | -0.48 | -2.07 | -1.41 | -2.83 | -0.92 | -2.01 | -1.09 |
| CO (Carbon monoxide)            | -1.50 | -1.90 | -1.33 | -2.67 | -0.46 | -1.93 | -1.09 |
| HCO (Formyl radical)            | 0.02 | -0.27 | 0.44 | -1.01 | 1.39 | -0.33 | 0.57 |
| CH₂O (Formaldehyde)             | -0.55 | -1.31 | -0.63 | -2.09 | 0.19 | -1.41 | -0.46 |
| CH₃OH (Methyl alcohol)          | -0.55 | -0.95 | -1.44 | -1.50 | -0.79 | -0.84 | -1.09 |
| Compound                  | ΔE (kJ/mol) | ΔE (kJ/mol) | ΔE (kJ/mol) | ΔE (kJ/mol) | ΔE (kJ/mol) | ΔE (kJ/mol) | ΔE (kJ/mol) |
|--------------------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|
| N₂ (Nitrogen diatomic)   | -2.24       | -2.80       | -1.55       | -3.56       | -0.71       | -2.88       | -1.28       |
| N₂H₄ (Hydrazine)         | -0.45       | -1.52       | -1.41       | -1.99       | -0.57       | -1.39       | -1.01       |
| NO (Nitric oxide)        | -0.42       | -0.92       | 0.60        | -1.52       | 1.44        | -1.12       | 0.87        |
| O₂ (Oxygen diatomic)     | -0.08       | -0.87       | 0.79        | -1.36       | 1.60        | -1.09       | 1.12        |
| H₂O₂ (Hydrogen peroxide) | -0.92       | -1.47       | -1.63       | -2.04       | -0.82       | -1.33       | -1.25       |
| F₂ (Fluorine diatomic)   | 0.42        | -0.38       | 1.69        | -0.57       | 2.42        | -0.73       | 2.15        |
| CO₂ (Carbon dioxide)     | -0.65       | -4.49       | -1.69       | -5.11       | -0.73       | -4.68       | -1.31       |
| P₂ (Phosphorus diatomic) | 0.48        | 0.33        | 0.73        | -0.46       | 1.71        | 0.35        | 0.95        |
| S₂ (Sulfur diatomic)     | 1.53        | 1.12        | 1.69        | 0.44        | 2.72        | 1.12        | 1.93        |
| Cl₂ (Chlorine diatomic)  | 0.75        | 0.38        | 1.06        | -0.33       | 1.99        | 0.27        | 1.33        |
| NaCl (Sodium Chloride)   | 0.65        | 0.52        | 0.16        | -0.16       | 0.79        | 0.65        | 0.46        |
| SiO (Silicon monoxide)   | 0.03        | -0.33       | 0.11        | -1.12       | 1.09        | -0.24       | 0.33        |
| CS (Carbon monosulfide)  | -0.09       | -0.30       | 0.33        | -1.03       | 1.25        | -0.33       | 0.54        |
| ClO (Monochlorine monoxide) | 2.19       | 1.60        | 2.58        | 1.06        | 3.37        | 1.41        | 2.77        |
| ClF (Chlorine monofluoride) | 0.44       | -0.14       | 0.92        | -0.79       | 1.85        | -0.22       | 1.28        |
| Si₂H₆ (Disilane)         | -0.69       | -1.22       | -1.58       | -1.69       | -0.76       | -1.17       | -1.20       |
| CH₃Cl (Methyl chloride)  | -0.51       | -0.84       | -1.39       | -1.47       | -0.68       | -0.76       | -1.01       |
| CH₃SH (Methanethiol)     | -0.50       | -0.87       | -1.41       | -1.44       | -0.63       | -0.79       | -1.03       |
| SO₂ (Sulfur dioxide)     | 0.81        | 0.41        | 1.41        | -0.19       | 2.42        | 0.30        | 1.66        |
| BF₃ (Borane, trifluoro-) | -1.04       | -1.25       | -1.71       | -1.88       | -0.82       | -1.17       | -1.31       |
| BCl₃ (Borane, trichloro-) | -0.17       | -1.01       | -0.16       | -1.52       | 0.76        | -0.98       | -0.03       |
| AlCl₃ (Aluminum trichloride) | 0.06       | -0.08       | -0.35       | -0.79       | 0.73        | -0.11       | -0.19       |
| CF₄ (Carbon tetrafluoride) | -1.33       | -1.96       | -2.48       | -2.53       | -1.52       | -1.82       | -2.04       |
| CCl₄ Carbon tetrachloride | -0.46       | -0.35       | -0.41       | -1.01       | 0.57        | -0.35       | -0.14       |
| OCS (Carbonyl sulfide)   | -0.74       | -1.58       | -1.03       | -2.26       | -0.08       | -1.58       | -0.82       |
| CS₂ (Carbon disulfide)   | 0.01        | -0.11       | 0.16        | -0.79       | 1.12        | -0.11       | 0.35        |
| CF₂O (Carbonic difluoride) | -2.37       | -2.50       | -1.55       | -3.40       | -0.65       | -2.42       | -1.36       |
| SiF₄ (Silicon tetrafluoride) | -0.81       | -1.25       | -1.66       | -1.88       | -0.63       | -1.22       | -1.22       |
| N₂O (Nitrous oxide)      | -2.01       | -2.58       | -1.58       | -3.26       | -0.65       | -2.75       | -1.36       |
| NF₃ (Nitrogen trifluoride) | -2.06       | -2.88       | -2.67       | -3.64       | -1.82       | -2.86       | -2.37       |
| PF₃ (Phosphorus trifluoride) | -1.23       | -1.58       | -1.88       | -2.12       | -0.98       | -1.50       | -1.55       |
| Compound                        | ΔH | D | ΔS | ΔG | D | ΔS | ΔG |
|--------------------------------|-----|---|----|----|---|----|----|
| O₃ (Ozone)                     | 1.93| 1.90| 3.24| 1.58| 4.22| 1.55| 3.48|
| F₂O (Difluorine monoxide)      | -0.31| -1.01| 0.44| -1.36| 1.22| -1.17| 0.82|
| ClF₃ (Chlorine trifluoride)    | 1.20| 0.63| 1.60| 0.14| 2.56| 0.52| 1.90|
| C₂F₄ (Tetrafluoroethylene)     | -1.65| -2.42| -2.07| -2.94| -1.03| -2.34| -1.66|
| CH₃CCH (Propyne)               | -1.13| -1.77| -1.41| -2.23| -0.82| -1.60| -1.06|
| CH₂CCH₂ (Allene)               | -0.56| -1.55| -1.60| -2.04| -0.92| -1.41| -1.22|
| C₃H₄ (Cyclopropene)            | -1.82| -2.01| -1.66| -2.80| -0.92| -2.07| -1.31|
| C₃H₆ (Cyclopropane)            | -0.65| -1.17| -1.71| -1.63| -1.03| -1.09| -1.33|
| CH₂F₂ (Methane, difluoro-)     | -0.58| -1.06| -1.52| -1.63| -0.95| -0.90| -1.20|
| CF₂H (Methane, trifluoro-)     | -0.60| -1.17| -1.58| -1.85| -1.01| -1.01| -1.25|
| CH₂Cl₂ (Methylene chloride)    | -0.49| -0.82| -1.31| -1.50| -0.49| -0.73| -0.98|
| CHCl₃ (Chloroform)             | -0.83| -0.79| -1.01| -1.52| -0.05| -0.73| -0.76|
| CH₃NO₂ (Methane, nitro-)       | -0.37| -0.49| 0.05| -1.06| 0.98| -0.65| 0.27|
| CH₃SiH₃ (Methyl silane)        | -0.53| -0.92| -1.47| -1.47| -0.73| -0.84| -1.09|
| HCOOH (Formic acid)            | -0.57| -2.15| -1.63| -2.88| -0.87| -2.18| -1.25|
| CH₃CONH₂ (Acetamide)           | -0.31| -1.60| -1.22| -2.09| -0.49| -1.44| -0.84|
| C₂N₂ (Cyanogen)                | -0.19| -0.33| 0.52| -1.03| 1.47| -0.38| 0.68|
| CH₂CO (Ketene)                 | -0.51| -1.41| -1.03| -1.96| -0.16| -1.28| -0.87|
| C₂H₄O (Ethylene oxide)         | -0.86| -1.03| -1.60| -1.55| -0.95| -0.95| -1.22|
| C₂H₂O₂ (Ethanedial)            | 0.69| 0.63| 1.28| -0.11| 2.18| 0.49| 1.41|
| CH₃CH₂OH (Ethanol)             | -0.53| -0.92| -1.44| -1.47| -0.76| -0.82| -1.09|
| CH₃OCH₃ (Dimethyl ether)        | -0.58| -1.01| -1.52| -1.47| -0.84| -0.90| -1.14|
| C₂H₄S (Thiirane)               | -0.78| -1.25| -1.60| -1.69| -0.87| -1.14| -1.20|
| CH₂CHF (Ethene, fluoro-)       | -0.88| -2.18| -1.66| -2.91| -1.01| -2.23| -1.28|
| CH₃CH₂Cl (Ethyl chloride)      | -0.51| -0.90| -1.47| -1.44| -0.73| -0.79| -1.09|
| CH₂CHCl (Ethene, chloro-)      | -1.11| -1.60| -1.41| -2.39| -0.52| -1.66| -1.20|
| CH₃CClO (Acetyl Chloride)      | -0.85| -1.12| -0.79| -1.80| 0.11| -1.14| -0.65|
| NO₂ (Nitrogen dioxide)         | 1.44| 0.90| 1.99| 0.38| 3.02| 0.76| 2.18|
| CFCl₃ (Trichloromonofluoromethane) | -0.68| -0.76| -0.65| -1.39| 0.33| -0.73| -0.41|
| CF₂Cl (Methane, chlorotrifluoro-) | -1.06| -1.63| -1.82| -2.28| -0.84| -1.55| -1.52|
| HCCF (Fluoroacetylene)         | -0.55| -0.95| -1.39| -1.47| -0.82| -0.82| -1.09|
| Molecule                      | Reference | ωM05-D | M05-2X | ωB97X-D |
|-------------------------------|-----------|--------|--------|---------|
| H (Hydrogen atom)             | 12.86     | 11.62  | 10.98  | 11.57   |
| He (Helium atom)              | 27.23     | 25.57  | 24.70  | 24.56   |
| Li (Lithium atom)             | 4.22      | 5.49   | 4.05   | 5.41    |
| Be (Beryllium atom)           | 9.66      | 8.70   | 6.94   | 8.57    |
| B (Boron atom)                | 7.99      | 6.83   | 5.11   | 6.66    |
| C (Carbon atom)               | 9.97      | 8.05   | 6.69   | 7.59    |
| N (Nitrogen atom)             | 14.74     | 11.97  | 10.47  | 11.61   |
| O (Oxygen atom)               | 12.14     | 9.63   | 8.54   | 9.00    |
| F (Fluorine atom)             | 13.98     | 10.88  | 10.28  | 9.74    |

TABLE XV: Reference values of FG115 database calculated by the CCSD(T) theory, compared with HOMO-LUMO gap results by DFT methods.
| Compound                  | Value1 | Value2 | Value3 | Value4 |
|--------------------------|--------|--------|--------|--------|
| Ne (Neon atom)           | 26.91  | 25.84  | 24.75  | 24.89  |
| Na (Sodium atom)         | 4.14   | 5.41   | 4.11   | 5.11   |
| Mg (Magnesium atom)      | 7.76   | 7.81   | 6.26   | 7.45   |
| Al (Aluminum atom)       | 5.53   | 5.11   | 3.32   | 5.11   |
| Si (Silicon atom)        | 6.73   | 5.88   | 4.11   | 5.74   |
| P (Phosphorus atom)      | 9.78   | 8.35   | 6.31   | 8.05   |
| S (Sulfur atom)          | 8.23   | 6.80   | 5.00   | 6.53   |
| Cl (Chlorine atom)       | 9.30   | 7.43   | 5.90   | 6.99   |
| Ar (Argon atom)          | 18.65  | 17.95  | 16.21  | 17.33  |
| CH₃ (Methyl radical)     | 9.86   | 8.87   | 6.83   | 8.54   |
| CH₄ (Methane)            | 15.06  | 14.69  | 13.52  | 14.14  |
| NH (Imidogen) (³Σ⁻)      | 13.17  | 11.32  | 9.85   | 10.80  |
| NH₂ (Amino radical)      | 11.34  | 10.09  | 8.62   | 9.63   |
| NH₃ (Ammonia)            | 11.54  | 11.53  | 10.17  | 10.85  |
| OH (Hydroxyl radical)    | 11.27  | 9.49   | 8.40   | 8.73   |
| H₂O (Water)              | 13.35  | 13.00  | 11.78  | 12.19  |
| HF (Hydrogen fluoride)   | 16.91  | 15.88  | 15.01  | 15.01  |
| SiH₃ (Silyl)             | 7.95   | 7.04   | 4.79   | 6.85   |
| SiH₄ (Silane)            | 14.03  | 13.55  | 12.13  | 13.08  |
| PH₃ (Phosphine)          | 11.82  | 11.29  | 9.74   | 10.85  |
| H₂S (Hydrogen sulfide)   | 11.00  | 10.99  | 9.47   | 10.50  |
| HCl (Hydrogen chloride)  | 13.36  | 13.00  | 11.56  | 12.43  |
| C₂H₂ (Acetylene)         | 13.43  | 12.13  | 10.93  | 11.59  |
| C₂H₄ (Ethylene)          | 12.57  | 11.75  | 10.09  | 11.07  |
| C₂H₆ (Ethane)            | 13.41  | 13.25  | 12.05  | 12.76  |
| HCN (Hydrogen cyanide)   | 14.31  | 14.04  | 12.89  | 13.44  |
| CO (Carbon monoxide)     | 15.57  | 14.31  | 12.97  | 13.90  |
| HCO (Formyl radical)     | 9.56   | 8.38   | 6.91   | 8.05   |
| CH₂O (Formaldehyde)      | 11.56  | 10.72  | 9.41   | 10.28  |
| CH₃OH (Methyl alcohol)   | 11.67  | 11.67  | 10.55  | 11.02  |
| N₂ (Nitrogen diatomic)   | 17.88  | 16.13  | 14.96  | 15.56  |
| Molecular Formula      | Value 1 | Value 2 | Value 3 | Value 4 |
|-----------------------|---------|---------|---------|---------|
| N₂H₄ (Hydrazine)      | 10.29   | 10.44   | 9.03    | 9.79    |
| NO (Nitric oxide)     | 10.11   | 8.11    | 6.91    | 7.48    |
| O₂ (Oxygen diatomic)  | 12.52   | 10.69   | 9.66    | 9.90    |
| H₂O₂ (Hydrogen peroxide) | 12.65 | 12.40   | 11.23   | 11.61   |
| F₂ (Fluorine diatomic)| 15.53   | 12.76   | 11.97   | 11.75   |
| CO₂ (Carbon dioxide)  | 14.58   | 14.66   | 13.27   | 13.95   |
| P₂ (Phosphorus diatomic)| 10.19| 9.19    | 7.43    | 8.95    |
| S₂ (Sulfur diatomic)  | 7.96    | 7.26    | 5.58    | 6.94    |
| Cl₂ (Chlorine diatomic)| 10.93 | 9.71    | 8.19    | 9.30    |
| NaCl (Sodium Chloride)| 8.64    | 8.43    | 7.15    | 7.94    |
| SiO (Silicon monoxide)| 11.60   | 10.77   | 9.11    | 10.44   |
| CS (Carbon monosulfide)| 11.58| 10.66   | 9.17    | 10.36   |
| ClO (Monochlorine monoxide)| 8.85| 7.53    | 6.34    | 7.13    |
| CIF (Chlorine monofluoride)| 12.43| 10.74   | 9.33    | 10.17   |
| Si₂H₆ (Disilane)      | 11.33   | 11.72   | 10.17   | 11.32   |
| CH₃Cl (Methyl chloride)| 12.01   | 12.00   | 10.66   | 11.42   |
| CH₃SH (Methanethiol)  | 10.01   | 10.20   | 8.68    | 9.71    |
| SO₂ (Sulfur dioxide)  | 11.74   | 10.36   | 8.87    | 9.93    |
| BF₃ (Borane, trifluoro-)| 17.22 | 16.54   | 15.53   | 15.59   |
| BCl₃ (Borane, trichloro-)| 12.07| 11.34   | 9.82    | 11.04   |
| AlCl₃ (Aluminum trichloride)| 12.13| 11.83   | 10.12   | 11.48   |
| CF₄ (Carbon tetrafluoride)| 17.85| 17.71   | 16.67   | 16.73   |
| CCl₄ (Carbon tetrachloride)| 11.97| 11.56   | 10.01   | 11.12   |
| OCS (Carbonyl sulfide)| 12.13   | 11.67   | 10.04   | 11.34   |
| CS₂ (Carbon disulfide)| 10.19   | 9.41    | 7.78    | 9.22    |
| CF₂O (Carbonic difluoride)| 16.08| 14.33   | 13.08   | 13.74   |
| SiF₄ (Silicon tetrafluoride)| 16.95| 17.03   | 15.88   | 16.08   |
| N₂O (Nitrous oxide)   | 15.01   | 13.57   | 12.16   | 13.11   |
| NF₃ (Nitrogen trifluoride)| 15.76| 15.29   | 14.17   | 14.69   |
| PF₃ (Phosphorus trifluoride)| 13.00| 12.62   | 11.15   | 12.24   |
| O₃ (Ozone)            | 11.06   | 9.11    | 7.70    | 8.49    |
| Compound                              | Value1  | Value2  | Value3  | Value4  |
|---------------------------------------|---------|---------|---------|---------|
| F₂O (Difluorine monoxide)             | 13.82   | 12.08   | 11.18   | 11.21   |
| ClF₃ (Chlorine trifluoride)           | 11.79   | 10.58   | 9.30    | 9.96    |
| C₂F₄ (Tetrafluoroethylene)            | 12.45   | 12.00   | 10.44   | 11.37   |
| CH₃CCH (Propyne)                      | 11.69   | 11.23   | 9.90    | 10.66   |
| CH₂CCH₂ (Allene)                      | 10.83   | 11.40   | 9.98    | 10.83   |
| C₃H₄ (Cyclopropene)                   | 11.87   | 10.99   | 9.52    | 10.42   |
| C₃H₆ (Cyclopropane)                   | 11.64   | 12.19   | 10.77   | 11.61   |
| CH₂F₂ (Methane, difluoro-)            | 14.15   | 13.79   | 12.92   | 13.16   |
| CF₃H (Methane, trifluoro-)            | 15.44   | 15.10   | 14.28   | 14.47   |
| CH₂Cl₂ (Methylene chloride)           | 12.18   | 12.16   | 10.77   | 11.70   |
| CHCl₃ (Chloroform)                    | 12.38   | 11.86   | 10.34   | 11.48   |
| CH₃NO₂ (Methane, nitro-)              | 11.94   | 11.07   | 9.79    | 10.44   |
| CH₃SiH₃ (Methyl silane)                | 12.35   | 12.70   | 11.23   | 12.21   |
| HCOOH (Formic acid)                   | 11.98   | 12.32   | 11.10   | 11.61   |
| CH₃CONH₂ (Acetamide)                  | 10.05   | 10.88   | 9.66    | 10.20   |
| C₂N₂ (Cyanogen)                       | 13.90   | 12.27   | 10.72   | 11.86   |
| CH₂CO (Ketene)                        | 10.32   | 10.23   | 8.65    | 9.87    |
| C₂H₄O (Ethylene oxide)                 | 11.68   | 11.86   | 10.74   | 11.12   |
| C₂H₂O₂ (Ethanediol)                   | 10.04   | 8.84    | 7.45    | 8.46    |
| CH₃CH₂OH (Ethanol)                    | 11.38   | 11.53   | 10.39   | 10.88   |
| CH₃OCH₃ (Dimethyl ether)               | 10.79   | 11.18   | 9.98    | 10.50   |
| C₂H₄S (Thiirane)                      | 9.93    | 10.17   | 8.73    | 9.66    |
| CH₂CHF (Ethene, fluoro-)              | 11.55   | 11.56   | 10.17   | 10.93   |
| CH₃CH₂Cl (Ethyl chloride)              | 11.74   | 11.91   | 10.58   | 11.37   |
| CH₂CHCl (Ethene, chloro-)             | 11.35   | 11.02   | 9.38    | 10.61   |
| CH₃COCl (Acetyl Chloride)             | 11.97   | 11.56   | 10.12   | 11.18   |
| NO₂ (Nitrogen dioxide)                 | 9.79    | 8.73    | 7.40    | 8.19    |
| CFCl₃ (Trichloromonofluoromethane)     | 12.61   | 11.89   | 10.34   | 11.48   |
| CF₃Cl (Methane, chlorotrifluoro-)      | 14.27   | 14.09   | 12.59   | 13.57   |
| HCCF (Fluoroacetylene)                 | 12.04   | 11.91   | 10.66   | 11.37   |
| HCCCN (Cyanoacetylene)                 | 12.20   | 11.26   | 9.71    | 10.93   |
| Compound                        | MSE   | MAE   | rms   |
|--------------------------------|-------|-------|-------|
| C<sub>4</sub>N<sub>2</sub> (2-Butynedinitrile) | 11.52 | 10.31 | 8.76  |
| C<sub>2</sub>N<sub>2</sub> (Cyanogen) | 13.90 | 12.27 | 10.72 |
| C<sub>3</sub>O<sub>2</sub> (Carbon suboxide) | 11.64 | 10.58 | 9.06  |
| FCN (Cyanogen fluoride)         | 14.33 | 13.76 | 12.21 |
| C<sub>4</sub>H<sub>2</sub> (Diacetylene) | 11.00 | 10.64 | 9.03  |
| H<sub>2</sub>CNS (Thioformaldehyde) | 9.18  | 8.05  | 6.47  |
| CHONH<sub>2</sub> (Formamide)   | 10.81 | 11.23 | 10.06 |
| CH<sub>2</sub>CCl<sub>2</sub> (Ethene, 1,1-dichloro-) | 11.17 | 10.69 | 9.06  |
| C<sub>2</sub>HF<sub>3</sub> (Trifluoroethylene) | 11.11 | 11.34 | 10.06 |
| CH<sub>2</sub>CF<sub>2</sub> (Ethene, 1,1-difluoro-) | 11.81 | 11.67 | 10.28 |
| CH<sub>3</sub>F (Methyl fluoride) | 14.09 | 13.71 | 12.76 |
| CF<sub>2</sub>Cl<sub>2</sub> (Difluorodichloromethane) | 13.33 | 12.81 | 11.29 |
| SiF<sub>2</sub> (Silicon difluoride) | 11.04 | 10.04 | 8.32  |

- **MSE**
- **MAE**
- **rms**
TABLE XVI: Experimental molecular geometries (in angstrom) for IP131, EA115 and FG115 databases collected from the NIST database \[86\]. The integers following the molecule are in order the spin multiplicities of neutral species, cation and anion. The molecules with only the spin multiplicity of the neutral species shown are in neither EA115 nor FG115 database. The spin multiplicities of neutral species are experimental values specified in the NIST database \[86\]. Each spin multiplicity of cations and anions is decided by CCSD(T)/aug-cc-pVTZ calculations, and corresponds to the lowest energy in between various spin multiplicities.

| Element          | Spin multiplicity of neutral species | Spin multiplicity of cation | Spin multiplicity of anion |
|------------------|--------------------------------------|----------------------------|-----------------------------|
| H (Hydrogen atom)| 2                                    | Null                       | 1                           |
| H                |                                      |                            |                             |
| He (Helium atom) | 1                                    | 2                          | 2                           |
| He               |                                      |                            |                             |
| Li (Lithium atom)| 2                                    | 1                          | 1                           |
| Li               |                                      |                            |                             |
| Be (Beryllium atom)| 1                                   | 2                          | 2                           |
| Be               |                                      |                            |                             |
| B (Boron atom)   | 2                                    | 1                          | 3                           |
| B                |                                      |                            |                             |
| C (Carbon atom)  | 3                                    | 2                          | 4                           |
| C                |                                      |                            |                             |
| N (Nitrogen atom)| 4                                    | 3                          | 3                           |
| N                |                                      |                            |                             |
| O (Oxygen atom)  | 3                                    | 4                          | 2                           |
| O                |                                      |                            |                             |
| F (Fluorine atom)| 2                                    | 3                          | 1                           |
| F                |                                      |                            |                             |
| Ne (Neon atom)   | 1                                    | 2                          | 2                           |
| Ne               |                                      |                            |                             |
| Element                  | Valency | Charge | Symbol      |
|-------------------------|---------|--------|-------------|
| Na (Sodium atom)        | 2       | 1      | Na          |
| Mg (Magnesium atom)     | 1       | 2      | Mg          |
| Al (Aluminum atom)      | 2       | 1      | Al          |
| Si (Silicon atom)       | 3       | 2      | Si          |
| P (Phosphorus atom)     | 4       | 3      | P           |
| S (Sulfur atom)         | 3       | 4      | S           |
| Cl (Chlorine atom)      | 2       | 3      | Cl          |
| Ar (Argon atom)         | 1       | 2      | Ar          |
| CH₃ (Methyl radical)    | 2       | 1      | CH₃         |
| CH₄ (Methane)           | 1       | 2      | CH₄         |
| NH (Imidogen) (³Σ⁻)     | 3       | 2      | NH          |

**CH₃ (Methyl radical)**

| Atom | x | y  | z    |
|------|---|----|------|
| Cl   | 0.0000 | 0.0000 | 0.0000 |
| H2   | 1.0790 | 0.0000 | 0.0000 |
| H3   | -0.5395 | -0.9344 | 0.0000 |
| H4   | -0.5395 | 0.9344  | 0.0000 |

**CH₄ (Methane)**

| Atom | x | y  | z    |
|------|---|----|------|
| Cl   | 0.0000 | 0.0000 | 0.0000 |
| H2   | 0.6276 | 0.6276 | 0.6276 |
| H3   | 0.6276 | -0.6276 | -0.6276 |
| H4   | -0.6276 | 0.6276  | -0.6276 |
| H5   | -0.6276 | -0.6276 | 0.6276 |

**NH (Imidogen) (³Σ⁻)**

| Atom | x | y  | z    |
|------|---|----|------|
| N1   | 0.0000 | 0.0000 | 0.0000 |
| H2   | 0.0000 | 0.0000 | 1.0362 |
| Molecular Structure | Index | X-Coordinates | Y-Coordinates | Z-Coordinates |
|---------------------|-------|---------------|---------------|---------------|
| NH\_2 (Amino radical) | 2 3 1 | 0.0000 | 0.0000 | 0.0000 |
| | | 0.0000 | 0.8036 | 0.6347 |
| | | 0.0000 | -0.8036 | 0.6347 |
| NH\_3 (Ammonia) | 1 2 2 | 0.0000 | 0.0000 | 0.0000 |
| | | 0.0000 | -0.9377 | -0.3816 |
| | | 0.8121 | 0.4689 | -0.3816 |
| | | -0.8121 | 0.4689 | -0.3816 |
| OH (Hydroxyl radical) | 2 3 1 | 0.0000 | 0.0000 | 0.0000 |
| | | 0.0000 | 0.0000 | 0.9697 |
| H\_2O (Water) | 1 2 2 | 0.0000 | 0.0000 | 0.1173 |
| | | 0.0000 | 0.7572 | -0.4692 |
| | | 0.0000 | -0.7572 | -0.4692 |
| HF (Hydrogen fluoride) | 1 2 2 | 0.0000 | 0.0000 | 0.0000 |
| | | 0.0000 | 0.0000 | 0.9168 |
| SiH\_3 (Silyl) | 2 1 1 | 0.0000 | 0.0000 | 0.0819 |
| | | 0.0000 | 1.3928 | -0.3820 |
| | | 1.2062 | -0.6964 | -0.3820 |
| | | -1.2062 | -0.6964 | -0.3820 |
| SiH\_4 (Silane) | 1 2 2 | 0.0000 | 0.0000 | 0.0000 |
| | | 0.8544 | 0.8544 | 0.8544 |
| | | -0.8544 | -0.8544 | 0.8544 |
| | | -0.8544 | 0.8544 | -0.8544 |
| Compound                  | X1  | Y1  | Z1  |
|--------------------------|-----|-----|-----|
| \( \text{PH}_3 \) (Phosphine) | 0.8544 | -0.8544 | -0.8544 |
| P1                       | 0.0000 | 0.0000 | 0.0000 |
| H2                       | 0.0000 | -1.1932 | -0.7717 |
| H3                       | 1.0333 | 0.5966 | -0.7717 |
| H4                       | -1.0333 | 0.5966 | -0.7717 |
| \( \text{H}_2\text{S} \) (Hydrogen sulfide) | 0.0000 | 0.0000 | 0.0000 |
| S1                       | 0.0000 | 0.0000 | 0.0000 |
| H2                       | 0.0000 | 0.9569 | 0.9208 |
| H3                       | 0.0000 | -0.9569 | 0.9208 |
| \( \text{HCl} \) (Hydrogen chloride) | 0.0000 | 0.0000 | 1.2746 |
| Cl1                      | 0.0000 | 0.0000 | 0.0000 |
| H2                       | 0.0000 | 0.0000 | 1.2746 |
| \( \text{C}_2\text{H}_2 \) (Acetylene) | 0.0000 | 0.0000 | 0.6013 |
| C1                       | 0.0000 | 0.0000 | 0.6013 |
| C2                       | 0.0000 | 0.0000 | -0.6013 |
| H3                       | 0.0000 | 0.0000 | 1.6644 |
| H4                       | 0.0000 | 0.0000 | -1.6644 |
| \( \text{C}_2\text{H}_4 \) (Ethylene) | 0.0000 | 0.0000 | 0.6695 |
| C1                       | 0.0000 | 0.0000 | 0.6695 |
| C2                       | 0.0000 | 0.0000 | -0.6695 |
| H3                       | 0.0000 | 0.9289 | 1.2321 |
| H4                       | 0.0000 | -0.9289 | 1.2321 |
| H5                       | 0.0000 | 0.9289 | -1.2321 |
| H6                       | 0.0000 | -0.9289 | -1.2321 |
| \( \text{C}_2\text{H}_6 \) (Ethane) | 0.0000 | 0.0000 | 0.7680 |
| C1                       | 0.0000 | 0.0000 | 0.7680 |
| C2                       | 0.0000 | 0.0000 | -0.7680 |
| H3                       | -1.0192 | 0.0000 | 1.1573 |
|        |        |        |        |
|--------|--------|--------|--------|
| H4     | 0.5096 | 0.8826 | 1.1573 |
| H5     | 0.5096 | -0.8826| 1.1573 |
| H6     | 1.0192 | 0.0000 | -1.1573|
| H7     | -0.5096| -0.8826| -1.1573|
| H8     | -0.5096| 0.8826 | -1.1573|
| HCN (Hydrogen cyanide) | 1 | 2 | 2 |
| C1     | 0.0000 | 0.0000 | 0.0000 |
| H2     | 0.0000 | 0.0000 | 1.0640 |
| N3     | 0.0000 | 0.0000 | -1.1560|
| CO (Carbon monoxide) | 1 | 2 | 2 |
| C1     | 0.0000 | 0.0000 | 0.0000 |
| O2     | 0.0000 | 0.0000 | 1.1283 |
| HCO (Formyl radical) | 2 | 1 | 1 |
| C1     | 0.0000 | 0.0000 | 0.0000 |
| H2     | 1.0800 | 0.0000 | 0.0000 |
| O3     | -0.5899| 1.0427 | 0.0000 |
| H₂CO (Formaldehyde) | 1 | 2 | 2 |
| O1     | 0.0000 | 0.0000 | 1.2050 |
| C2     | 0.0000 | 0.0000 | 0.0000 |
| H3     | 0.0000 | 0.9429 | -0.5876|
| H4     | 0.0000 | -0.9429| -0.5876|
| CH₃OH (Methyl alcohol) | 1 | 2 | 2 |
| C1     | -0.0503| 0.6685 | 0.0000 |
| O2     | -0.0503| -0.7585| 0.0000 |
| H3     | -1.0807| 1.0417 | 0.0000 |
| H4     | 0.4650 | 1.0417 | 0.8924 |
| H5     | 0.4650 | 1.0417 | -0.8924|
| H6     | 0.8544 | -1.0677| 0.0000 |
| N₂ (Nitrogen diatomic) | 1 | 2 | 2 |
| Molecule                | u   | v   | w   | Energy  |
|-------------------------|-----|-----|-----|---------|
| N$_2$H$_4$ (Hydrazine)  | 0.0000 | 0.0000 | 0.5488 |
|                         | 0.0000 | 0.0000 | -0.5488 |
| NO (Nitric oxide)       | 0.0000 | 0.0000 | 1.1508 |
|                         | 0.0000 | 0.0000 | 0.0000 |
| O$_2$ (Oxygen diatomic) | 0.0000 | 0.0000 | 1.2075 |
|                         | 0.0000 | 0.0000 | 0.0000 |
| H$_2$O$_2$ (Hydrogen peroxide) | 0.0000 | 0.0000 | 0.7375 |
|                         | 0.0000 | 0.0000 | -0.0528 |
| F$_2$ (Fluorine diatomic) | 0.0000 | 0.0000 | 1.4119 |
| CO$_2$ (Carbon dioxide) | 0.0000 | 0.0000 | 1.1621 |
|                         | 0.0000 | 0.0000 | -1.1621 |
| P$_2$ (Phosphorus diatomic) | 0.0000 | 0.0000 | 0.0000 |
| Molecule                    | Type | Coordinates | Energy  |
|-----------------------------|------|-------------|---------|
| П2                          |      |             | 1.8934  |
| $S_2$ (Sulfur diatomic) ($^3\Sigma_g$) | 3 2 2 |             |         |
| S1                          |      | 0.0000      | 0.0000  |
| S2                          |      | 0.0000      | 1.8892  |
| Cl₂ (Chlorine diatomic)     | 1 2 2 |             |         |
| Cl1                         |      | 0.0000      | 0.0000  |
| Cl2                         |      | 0.0000      | 1.9879  |
| NaCl (Sodium Chloride)      | 1 2 2 |             |         |
| Na1                         |      | 0.0000      | 0.0000  |
| Cl₂                         |      | 0.0000      | 2.3608  |
| SiO (Silicon monoxide)      | 1 2 2 |             |         |
| Si1                         |      | 0.0000      | 0.0000  |
| O₂                          |      | 0.0000      | 1.5097  |
| CS (Carbon monosulfide)     | 1 2 2 |             |         |
| C1                          |      | 0.0000      | 0.0000  |
| S₂                          |      | 0.0000      | 1.5349  |
| ClO (Monochlorine monoxide) | 2 3 1 |             |         |
| O₁                          |      | 0.0000      | 0.0000  |
| Cl₂                         |      | 0.0000      | 1.5696  |
| ClF (Chlorine monofluoride) | 1 2 2 |             |         |
| F₁                          |      | 0.0000      | 0.0000  |
| Cl₂                         |      | 0.0000      | 1.6283  |
| Si₂H₆ (Disilane)            | 1 2 2 |             |         |
| Si₁                         |      | 0.0000      | 1.1600  |
| Si₂                         |      | 0.0000      | -1.1600 |
| H₃                          |      | 0.0000      | 1.3865  |
| H₄                          |      | -1.2008     | -0.6933 |
| H₅                          |      | 1.2008      | -0.6933 |
| H₆                          |      | 0.0000      | -1.3865 |
|     |   |   |   |   |   |   |
|-----|---|---|---|---|---|---|
| H7  | -1.2008 | 0.6933 | -1.6483 |
| H8  | 1.2008   | 0.6933 | -1.6483 |

**CH₃Cl (Methyl chloride) 1 2 2**

|     |   |   |   |   |
|-----|---|---|---|---|
| C1  | 0.0000   | 0.0000 | 0.0000 |
| Cl₂ | 0.0000   | 0.0000 | 1.7810 |
| H3  | 1.0424   | 0.0000 | -0.3901 |
| H4  | -0.5212  | 0.9027 | -0.3901 |
| H5  | -0.5212  | -0.9027| -0.3901 |

**CH₃SH (Methanethiol) 1 2 2**

|     |   |   |   |   |   |   |
|-----|---|---|---|---|---|---|
| C1  | -0.8500 | -0.0344 | -0.2000 |
| S2  | 0.9000  | -0.5125 | -0.1219 |
| H3  | 1.4219  | 0.5781  | 0.4250  |
| H4  | -0.9406 | 0.8688  | -0.8219 |
| H5  | -1.4219 | -0.8688 | -0.6469 |
| H6  | -1.2031 | 0.1656  | 0.8219  |

**SO₂ (Sulfur dioxide) 1 2 2**

|     |   |   |   |   |
|-----|---|---|---|---|
| S1  | 0.0000   | 0.0000 | 0.0000 |
| O₂  | 0.0000   | 1.2371 | 0.7215 |
| O₃  | 0.0000   | -1.2371| 0.7215 |

**BF₃ (Borane, trifluoro-) 1 2 2**

|     |   |   |   |   |
|-----|---|---|---|---|
| B1  | 0.0000   | 0.0000 | 0.0000 |
| F2  | 0.0000   | 1.3070 | 0.0000 |
| F3  | 1.1319   | -0.6535| 0.0000 |
| F4  | -1.1319  | -0.6535| 0.0000 |

**BCl₃ (Borane, trichloro-) 1 2 2**

|     |   |   |   |   |
|-----|---|---|---|---|
| B1  | 0.0000   | 0.0000 | 0.0000 |
| Cl₂ | 0.0000   | 1.7421 | 0.0000 |
| Cl₃ | 1.5087   | -0.8711| 0.0000 |
| Cl₄ | -1.5087  | -0.8711| 0.0000 |
| Molecular Formula | Atom | x-coordinate | y-coordinate | z-coordinate |
|-------------------|------|--------------|--------------|--------------|
| **AlCl₃ (Aluminum trichloride)** | Al1 | 0.0000 | 0.0000 | 0.0000 |
|                   | Cl2 | 0.0000 | 2.0600 | 0.0000 |
|                   | Cl3 | 1.7840 | -1.0300 | 0.0000 |
|                   | Cl4 | -1.7840 | -1.0300 | 0.0000 |
| **CF₄ (Carbon tetrafluoride)** | C1  | 0.0000 | 0.0000 | 0.0000 |
|                   | F2  | 0.7593 | 0.7593 | 0.7593 |
|                   | F3  | -0.7593 | -0.7593 | 0.7593 |
|                   | F4  | -0.7593 | 0.7593 | -0.7593 |
|                   | F5  | 0.7593 | -0.7593 | -0.7593 |
| **CCl₄ (Carbon tetrachloride)** | C1  | 0.0000 | 0.0000 | 0.0000 |
|                   | Cl2 | 1.0202 | 1.0202 | 1.0202 |
|                   | Cl3 | -1.0202 | -1.0202 | 1.0202 |
|                   | Cl4 | -1.0202 | 1.0202 | -1.0202 |
|                   | Cl5 | 1.0202 | -1.0202 | -1.0202 |
| **OCS (Carbonyl sulfide)** | C1  | 0.0000 | 0.0000 | 0.0000 |
|                   | O2  | 0.0000 | 0.0000 | 1.1600 |
|                   | S3  | 0.0000 | 0.0000 | -1.5600 |
| **CS₂ (Carbon disulfide)** | C1  | 0.0000 | 0.0000 | 0.0000 |
|                   | S2  | 0.0000 | 0.0000 | 1.5540 |
|                   | S3  | 0.0000 | 0.0000 | -1.5540 |
| **CF₂O (Carbonic difluoride)** | O1  | 0.0000 | 0.0000 | 1.3143 |
|                   | C2  | 0.0000 | 0.0000 | 0.1403 |
|                   | F3  | 0.0000 | 1.0614 | -0.6309 |
|     |        |        |        |        |
|-----|--------|--------|--------|--------|
| F4  | 0.0000 | -1.0614 | -0.6309 |
| SiF₄ (Silicon tetrafluoride) 1 2 2 |
| Si1 | 0.0000 | 0.0000 | 0.0000 |
| F2  | 0.8972 | 0.8972 | 0.8972 |
| F3  | -0.8972 | -0.8972 | 0.8972 |
| F4  | -0.8972 | 0.8972 | -0.8972 |
| F5  | 0.8972 | -0.8972 | -0.8972 |
| N₂O (Nitrous oxide) 1 2 2 |
| N1  | 0.0000 | 0.0000 | -1.1998 |
| N2  | 0.0000 | 0.0000 | -0.0716 |
| O3  | 0.0000 | 0.0000 | 1.1126 |
| NF₃ (Nitrogen trifluoride) 1 2 2 |
| N1  | 0.0000 | 0.0000 | 0.4731 |
| F2  | 0.0000 | 1.2279 | -0.1226 |
| F3  | 1.0634 | -0.6140 | -0.1226 |
| F4  | -1.0634 | -0.6140 | -0.1226 |
| PF₃ (Phosphorus trifluoride) 1 2 2 |
| P1  | 0.0000 | 0.0000 | 0.4602 |
| F2  | 0.0000 | 1.3578 | -0.2557 |
| F3  | 1.1759 | -0.6789 | -0.2557 |
| F4  | -1.1759 | -0.6789 | -0.2557 |
| O₃ (Ozone) 1 2 2 |
| O1  | 0.0000 | 0.0000 | 0.0000 |
| O2  | 0.0000 | 1.0885 | 0.6697 |
| O3  | 0.0000 | -1.0885 | 0.6697 |
| F₂O (Difluorine monoxide) 1 2 2 |
| O1  | 0.0000 | 0.0000 | 0.6074 |
| F2  | 0.0000 | 1.1063 | -0.2700 |
| F3  | 0.0000 | -1.1063 | -0.2700 |
| Compound                        | 1   | 2   | 3   |
|--------------------------------|-----|-----|-----|
| **ClF₃ (Chlorine trifluoride)** | 1   | 2   | 2   |
| Cl1                            | 0.0000 | 0.0000 | 0.3572 |
| F2                             | 0.0000 | 0.0000 | -1.2408 |
| F3                             | 0.0000 | 1.6964 | 0.2831 |
| F4                             | 0.0000 | -1.6964 | 0.2831 |
| **C₂F₄ (Tetrafluoroethylene)**  | 1   | 2   | 2   |
| C1                             | 0.0000 | 0.0000 | 0.6555 |
| C2                             | 0.0000 | 0.0000 | -0.6555 |
| F3                             | 0.0000 | 1.0961 | 1.3893 |
| F4                             | 0.0000 | -1.0961 | 1.3893 |
| F5                             | 0.0000 | -1.0961 | -1.3893 |
| F6                             | 0.0000 | 1.0961 | -1.3893 |
| **CF₃CN (Acetonitrile, trifluoro-)** | 1   |   |   |
| C1                             | 0.0000 | 0.0000 | -0.3406 |
| C2                             | 0.0000 | 0.0000 | 1.1518 |
| N3                             | 0.0000 | 0.0000 | 2.3054 |
| F4                             | 0.0000 | 1.2540 | -0.7780 |
| F5                             | 1.0860 | -0.6270 | -0.7780 |
| F6                             | -1.0860 | -0.6270 | -0.7780 |
| **CH₃CCH (Propyne)**           | 1   | 2   | 2   |
| C1                             | 0.0000 | 0.0000 | -1.2455 |
| C2                             | 0.0000 | 0.0000 | 0.2135 |
| C3                             | 0.0000 | 0.0000 | 1.4195 |
| H4                             | 0.0000 | 0.0000 | 2.4755 |
| H5                             | 0.0000 | 1.0465 | -1.6003 |
| H6                             | 0.9063 | -0.5232 | -1.6003 |
| H7                             | -0.9063 | -0.5232 | -1.6003 |
| **CH₂CCH₂ (Allene)**           | 1   | 2   | 2   |
| C1                             | 0.0000 | 0.0000 | 0.0000 |
|   | X  | Y  | Z  |   |
|---|----|----|----|---|
| C2 | 0.0000 | 0.0000 | 1.3080 |   |
| C3 | 0.0000 | 0.0000 | -1.3080 |   |
| H4 | 0.0000 | 0.9327 | 1.8662 |   |
| H5 | 0.0000 | -0.9327 | 1.8662 |   |
| H6 | 0.9327 | 0.0000 | -1.8662 |   |
| H7 | -0.9327 | 0.0000 | -1.8662 |   |

**C₃H₄ (Cyclopropene)**

|   | X  | Y  | Z  |   |
|---|----|----|----|---|
| C1 | 0.0000 | 0.0000 | 0.8628 |   |
| C2 | 0.0000 | 0.6476 | -0.5001 |   |
| C3 | 0.0000 | -0.6476 | -0.5001 |   |
| H4 | 0.0000 | 1.5745 | -1.0386 |   |
| H5 | 0.0000 | -1.5745 | -1.0386 |   |
| H6 | 0.9154 | 0.0000 | 1.4509 |   |
| H7 | -0.9154 | 0.0000 | 1.4509 |   |

**C₃H₆ (Cyclopropane)**

|   | X  | Y  | Z  |   |
|---|----|----|----|---|
| C1 | 0.0000 | 0.8666 | 0.0000 |   |
| C2 | 0.7505 | -0.4333 | 0.0000 |   |
| C3 | -0.7505 | -0.4333 | 0.0000 |   |
| H4 | 0.0000 | 1.4525 | 0.9108 |   |
| H5 | 1.2579 | -0.7262 | 0.9108 |   |
| H6 | -1.2579 | -0.7262 | 0.9108 |   |
| H7 | 0.0000 | 1.4525 | -0.9108 |   |
| H8 | 1.2579 | -0.7262 | -0.9108 |   |
| H9 | -1.2579 | -0.7262 | -0.9108 |   |

**C₃H₈ (Propane)**

|   | X  | Y  | Z  |   |
|---|----|----|----|---|
| C1 | 0.0000 | 0.5863 | -0.0000 |   |
| C2 | -1.2681 | -0.2626 | 0.0000 |   |
| C3 | 1.2681 | -0.2626 | -0.0000 |   |
| H4 | 0.0000 | 1.2449 | 0.8760 |   |
|  |  |  |  |
|---|---|---|---|
| H5  | -0.0003 | 1.2453 | -0.8758 |
| H6  | -2.1576 | 0.3742 | 0.0000 |
| H7  | 2.1576  | 0.3743 | -0.0000 |
| H8  | -1.3271 | -0.9014 | 0.8800 |
| H9  | -1.3271 | -0.9014 | -0.8800 |
| H10 | 1.3271  | -0.9014 | -0.8800 |
| H11 | 1.3272  | -0.9014 | 0.8800 |

CH$_3$CCCH$_3$ (2-Butyne)  1

|  |  |  |  |
|---|---|---|---|
| C1 | 0.0000 | 0.0000 | 0.6070 |
| C2 | 0.0000 | 0.0000 | -0.6070 |
| C3 | 0.0000 | 0.0000 | 2.0750 |
| C4 | 0.0000 | 0.0000 | -2.0750 |
| H5 | 0.0000 | 1.0440 | 2.4695 |
| H6 | -0.9041 | -0.5220 | 2.4695 |
| H7 | 0.9041  | -0.5220 | 2.4695 |
| H8 | 0.0000  | 1.0440  | -2.4695 |
| H9 | 0.9041  | -0.5220 | -2.4695 |
| H10| -0.9041 | -0.5220 | -2.4695 |

C$_4$H$_6$ (Cyclobutene)  1

|  |  |  |  |
|---|---|---|---|
| C1 | 0.0000 | 0.6710 | 0.8107 |
| C2 | 0.0000 | -0.6710 | 0.8107 |
| C3 | 0.0000 | 0.7821 | -0.7023 |
| C4 | 0.0000 | -0.7821 | -0.7023 |
| H5 | 0.0000 | 1.4165 | 1.5962 |
| H6 | 0.0000 | -1.4165 | 1.5962 |
| H7 | 0.8986 | 1.2425 | -1.1233 |
| H8 | -0.8986 | -1.2425 | -1.1233 |
| H9 | -0.8986 | 1.2425  | -1.1233 |
| H10| 0.8986 | -1.2425 | -1.1233 |
### CH₃CH(CH₃)CH₃ (Isobutane) 1

|   | C1   | H2   | C3   | C4   | C5   | H6   | H7   | H8   | H9   | H10  | H11  | H12  | H13  | H14  |
|---|------|------|------|------|------|------|------|------|------|------|------|------|------|------|
|   | 0.000| 0.000| 0.000| 1.4528| -1.2582| 0.0000| 1.2875| -1.2875| 0.8941| -0.8941| 1.2482| 2.1422| -2.1422| -1.2482|
|   |      |      |      | -0.7264| -0.7264| 1.4867| -0.7433| -0.7433| 1.9575| 1.9575| -1.7530| -0.2045| -0.2045| -1.7530|
|   |      |      |      |       |       |      |      |      |      |      |      |      |      |      |
|   | 0.3650| 1.4730| -0.0987| -0.0987| -0.0987| -1.1931| -1.1931| -1.1931| 0.2821| 0.2821| 0.2821| 0.2821| 0.2821| 0.2821|

### C₆H₆ (Benzene) 1

|   | C1   | C2   | C3   | C4   | C5   | C6   | H7   | H8   | H9   | H10  | H11  | H12  | H13  | H14  |
|---|------|------|------|------|------|------|------|------|------|------|------|------|------|------|
|   | 0.000| 1.2098| 1.2098| 0.0000| -1.2098| -1.2098| 0.0000| 2.1486| 2.1486| 0.0000| 0.0000| 0.0000| 0.0000| 0.0000|
|   |      | 0.6985| -0.6985|      | -0.6985| 0.6985|      | 2.4810| 1.2405|      |      |      |      |      |
|   |      |      |      |      |      |      |      |      |      |      |      |      |      |      |
|   |      |      |      |      |      |      |      |      |      |      |      |      |      |      |
|   | 0.0000| 0.0000| 0.0000| 0.0000| 0.0000| 0.0000| 0.0000| 0.0000| 0.0000| 0.0000| 0.0000| 0.0000| 0.0000| 0.0000|

### CH₃F₂ (Methane, difluoro-) 1 2 2
| Molecule                        | C1          | H2          | H3          | F4          | F5          |
|--------------------------------|-------------|-------------|-------------|-------------|-------------|
| CHF₃ (Methane, trifluoro-)     | 0.0000      | 0.0000      | 0.5003      |             |             |
|                                | -0.9029     | 0.0000      | 1.1002      |             |             |
|                                | 0.9029      | 0.0000      | 1.1002      |             |             |
|                                | 0.0000      | 1.0962      | -0.2890     |             |             |
|                                | 0.0000      | -1.0962     | -0.2890     |             |             |
| CH₂Cl₂ (Methylene chloride)    | 0.0000      | 0.0000      | 0.3086      |             |             |
|                                | -0.8854     | 0.0000      | 1.3734      |             |             |
|                                | 0.8854      | 0.0000      | 1.3734      |             |             |
|                                | 0.0000      | 1.2609      | -0.1207     |             |             |
|                                | 1.0920      | -0.6305     | -0.1207     |             |             |
|                                | -1.0920     | -0.6305     | -0.1207     |             |             |
| CHCl₃ (Chloroform)             | 0.0000      | 0.0000      | 0.7761      |             |             |
|                                | -0.8854     | 0.0000      | 1.3734      |             |             |
|                                | 0.8854      | 0.0000      | 1.3734      |             |             |
|                                | 0.0000      | 1.4675      | -0.2178     |             |             |
|                                | 1.4343      | -0.8281     | -0.0928     |             |             |
|                                | -1.4343     | -0.8281     | -0.0928     |             |             |
| CH₃NO₂ (Methane, nitro-)       | 1.4008      | 0.0000      | 0.0000      |             |             |
|                                | -0.0878     | 0.0000      | 0.0000      |             |             |
|                                | 1.7215      | -1.0392     | 0.0000      |             |             |
|                                | 1.7215      | 0.5196      | 0.0000      |             |             |
|                                | 1.7215      | 0.5196      | -0.9000     |             |             |
| CH₃SiH₃ (Methyl silane) | 1  | 2  | 2 |
|------------------------|----|----|---|
| C1                     | 0.0000 | 0.0000 | -1.2367 |
| Si2                    | 0.0000 | 0.0000 | 0.6319 |
| H3                     | 0.0000 | -1.0237 | -1.6272 |
| H4                     | -0.8866 | 0.5119 | -1.6272 |
| H5                     | 0.8866 | 0.5119 | -1.6272 |
| H6                     | 0.0000 | 1.3893 | 1.1514 |
| H7                     | -1.2031 | -0.6946 | 1.1514 |
| H8                     | 1.2031 | -0.6946 | 1.1514 |

| HCOOH (Formic acid)    | 1  | 2  | 2 |
|------------------------|----|----|---|
| C1                     | 0.0000 | 0.4199 | 0.0000 |
| O2                     | -1.0543 | -0.4121 | 0.0000 |
| O3                     | 1.1506 | 0.0721 | 0.0000 |
| H4                     | -0.0799 | 1.5140 | 0.0000 |
| H5                     | -0.6905 | -1.3134 | 0.0000 |

| CH₃CONH₂ (Acetamide)   | 1  | 2  | 2 |
|------------------------|----|----|---|
| C1                     | -1.3674 | -0.3302 | 0.0013 |
| C2                     | 0.0720 | 0.1552 | -0.0019 |
| N3                     | 1.0259 | -0.8416 | -0.0326 |
| O4                     | 0.3726 | 1.3376 | 0.0057 |
| H5                     | -2.0656 | 0.5484 | -0.0612 |
| H6                     | -1.5426 | -1.0080 | -0.8780 |
| H7                     | -1.5719 | -0.9088 | 0.9430 |
| H8                     | 2.0050 | -0.5675 | 0.0710 |
| H9                     | 0.7853 | -1.8244 | 0.1113 |

| C₂H₅N (Aziridine)      | 1  |
|------------------------|----|
| N1                     | -0.0037 | 0.8559 | -0.1934 |
|   |      |      |      |
|---|------|------|------|
| H2 | -0.0140 | 1.4040 | 0.6620 |
| C3 | -0.7380 | -0.4043 | 0.0261 |
| C4 | 0.7425  | -0.3952 | 0.0380 |
| H5 | -1.2757 | -0.4486 | 0.9652 |
| H6 | -1.2332 | -0.8641 | -0.8216|
| H7 | 1.2820  | -0.7584 | -0.8280|
| H8 | 1.2404  | -0.5270 | 0.9918 |

C₂N₂ (Cyanogen) 1 2 2
|   |      |      |      |
|---|------|------|------|
| C1 | 0.0000 | 0.0000 | 0.6950 |
| C2 | 0.0000 | 0.0000 | -0.6950|
| N3 | 0.0000 | 0.0000 | 1.8450 |
| N4 | 0.0000 | 0.0000 | -1.8450|

CH₃NHCH₃ (Dimethylamine) 1
|   |      |      |      |
|---|------|------|------|
| N1 | 0.0934 | -0.5520 | 0.0000 |
| H2 | -0.6454 | -1.2544 | 0.0000 |
| C3 | -0.0220 | 0.2554  | 1.2139 |
| C4 | -0.0220 | 0.2554  | -1.2139|
| H5 | -0.9221 | 0.8833  | 1.2437 |
| H6 | -0.9221 | 0.8833  | -1.2437|
| H7 | 0.8440  | 0.9287  | 1.2609 |
| H8 | 0.8440  | 0.9287  | -1.2609|
| H9 | -0.0138 | -0.3909 | 2.0843 |
| H10| -0.0138 | -0.3909 | -2.0843|

CH₂CO (Ketene) 1 2 2
|   |      |      |      |
|---|------|------|------|
| C1 | 0.0000 | 0.0000 | 0.0000 |
| C2 | 0.0000 | 0.0000 | 1.3150 |
| O3 | 0.0000 | 0.0000 | 2.4750 |
| H4 | 0.0000 | 0.9451 | -0.5206|
| H5 | 0.0000 | -0.9451| -0.5206|
| Compound          | Atom | X    | Y    | Z    |
|-------------------|------|------|------|------|
| C₂H₄O (Ethylene oxide) | O1   | 0.0000 | 0.0000 | 0.8517 |
|                   | C2   | 0.0000 | 0.7297 | -0.3725 |
|                   | C3   | 0.0000 | -0.7297 | -0.3725 |
|                   | H4   | -0.9230 | 1.2565 | -0.5859 |
|                   | H5   | 0.9230 | 1.2565 | -0.5859 |
|                   | H6   | 0.9230 | -1.2565 | -0.5859 |
|                   | H7   | -0.9230 | -1.2565 | -0.5859 |
| C₂H₂O₂ (Ethanediol) | C1   | 0.0000 | 0.7630 | 0.0000 |
|                   | C2   | 0.0000 | -0.7630 | 0.0000 |
|                   | H3   | 1.0481 | 1.1907 | 0.0000 |
|                   | H4   | -1.0481 | -1.1907 | 0.0000 |
|                   | O5   | -1.0367 | 1.3908 | 0.0000 |
|                   | O6   | 1.0367 | -1.3908 | 0.0000 |
| CH₃CH₂OH (Ethanol) | C1   | 1.1879 | -0.3829 | 0.0000 |
|                   | C2   | 0.0000 | 0.5526 | 0.0000 |
|                   | O3   | -1.1867 | -0.2472 | 0.0000 |
|                   | H4   | -1.9237 | 0.3850 | 0.0000 |
|                   | H5   | 2.0985 | 0.2306 | 0.0000 |
|                   | H6   | 1.1184 | -1.0093 | 0.8869 |
|                   | H7   | 1.1184 | -1.0093 | -0.8869 |
|                   | H8   | -0.0227 | 1.1812 | 0.8852 |
|                   | H9   | -0.0227 | 1.1812 | -0.8852 |
| CH₃OCH₃ (Dimethyl ether) | O1   | 0.0000 | 0.0000 | 0.5952 |
|                   | C2   | 0.0000 | 1.1669 | -0.1963 |
|                   | C3   | 0.0000 | -1.1669 | -0.1963 |
|   | H4    | H5    | H6    | H7    | H8    | H9    |
|---|-------|-------|-------|-------|-------|-------|
|   | 0.0000| 2.0489| 0.4542|       |       |       |
|   | 0.0000| -2.0489| 0.4542|       |       |       |
|   | 0.8950| 1.1787| -0.8287|       |       |       |
|   | -0.8950| 1.1787| -0.8287|       |       |       |
|   | -0.8950| -1.1787| -0.8287|       |       |       |
|   | 0.8950| -1.1787| -0.8287|       |       |       |

| C₂H₄S (Thiirane) | 1 | 2 | 2 |
|---|---|---|---|
| S1 | 0.0000 | 0.0000 | 0.8622 |
| C2 | 0.0000 | 0.7421 | -0.7942 |
| C3 | 0.0000 | -0.7421 | -0.7942 |
| H4 | -0.9174 | 1.2493 | -1.0661 |
| H5 | 0.9174 | 1.2493 | -1.0661 |
| H6 | 0.9174 | -1.2493 | -1.0661 |
| H7 | -0.9174 | -1.2493 | -1.0661 |

| CH₃SOCH₃ (Dimethyl sulfoxide) | 1 |
|---|---|
| S1 | 0.0000 | 0.1432 | 0.4202 |
| O2 | 0.0000 | 1.4024 | -0.3667 |
| C3 | 1.3425 | -0.8664 | -0.2227 |
| C4 | -1.3425 | -0.8664 | -0.2227 |
| H5 | 2.2553 | -0.4311 | 0.0751 |
| H6 | -2.2553 | -0.4311 | 0.0751 |
| H7 | 1.3057 | -1.8579 | 0.2349 |
| H8 | 1.2255 | -0.9383 | -1.3113 |
| H9 | -1.3057 | -1.8579 | 0.2349 |
| H10 | -1.2255 | -0.9383 | -1.3113 |

| CH₂CHF (Ethene, fluoro-) | 1 | 2 | 2 |
|---|---|---|---|
| C1 | 0.0000 | 0.4476 | 0.0000 |
| C2 | 1.1877 | -0.1487 | 0.0000 |
| F3 | -1.1356 | -0.2769 | 0.0000 |
| Atom   | X   | Y   | Z   |
|--------|-----|-----|-----|
| H4     | -0.2349 | 1.5038 | 0.0000 |
| H5     | 1.2321   | -1.2348 | 0.0000 |
| H6     | 2.0966   | 0.4290  | 0.0000 |
| C1     | 1.5949   | -0.3563 | -0.0000 |
| C2     | 0.4757   | 0.6568  | -0.0004 |
| H3     | 2.5527   | 0.1648  | 0.0000 |
| H4     | 1.5351   | -0.9919 | -0.8828 |
| H5     | 1.5347   | -0.9917 | 0.8828 |
| Cl6    | -1.1206  | -0.1505 | -0.0005 |
| H7     | 0.5089   | 1.2945  | -0.8790 |
| H8     | 0.4949   | 1.2796  | 0.8893 |
| C1     | 0.0000   | 0.0000  | 1.3320 |
| C2     | 1.4961   | 0.6994  | 0.0000 |
| O3     | -0.8349  | 1.3710  | 0.0000 |
| Cl4    | -0.4665  | -1.2092 | 0.0000 |
| H5     | 1.7591   | 1.7726  | 0.0000 |
| H6     | 1.9367   | 0.2285  | 0.8973 |
| H7     | 1.9367   | 0.2285  | -0.8973 |
| Cl1    | 1.7375   | 0.1388  | 0.0000 |
|       | X       | Y       | Z       |
|-------|---------|---------|---------|
| C2    | 0.0000  | 0.5937  | 0.0000  |
| H3    | -0.1639 | 1.2199  | 0.9054  |
| H4    | -0.1639 | 1.2199  | -0.9054 |
| C5    | -0.8957 | -0.6405 | 0.0000  |
| H6    | -0.6638 | -1.2607 | 0.8947  |
| H7    | -0.6638 | -1.2607 | -0.8947 |
| C8    | -2.3710 | -0.2543 | 0.0000  |
| H9    | -2.6338 | 0.3458  | 0.8998  |
| H10   | -2.6338 | 0.3458  | -0.8998 |
| H11   | -3.0133 | -1.1633 | 0.0000  |

N(CH₃)₃ (Trimethylamine)  1

|       | X       | Y       | Z       |
|-------|---------|---------|---------|
| N1    | 0.0000  | -0.0000 | -0.3852 |
| C2    | -0.9758 | -0.9757 | 0.0634  |
| C3    | 1.3330  | -0.3571 | 0.0634  |
| C4    | -0.3572 | 1.3328  | 0.0634  |
| H5    | -1.0253 | -1.0252 | 1.1492  |
| H6    | 1.4006  | -0.3752 | 1.1492  |
| H7    | -0.3753 | 1.4004  | 1.1492  |
| H8    | -1.9833 | -0.7091 | -0.3156 |
| H9    | -0.7093 | -1.9833 | -0.3156 |
| H10   | 1.6060  | -1.3629 | -0.3156 |
| H11   | 2.0722  | 0.3776  | -0.3156 |
| H12   | 0.3774  | 2.0722  | -0.3156 |
| H13   | -1.3631 | 1.6057  | -0.3156 |

C₄H₄O (Furan)  1

|       | X       | Y       | Z       |
|-------|---------|---------|---------|
| O1    | 0.0000  | 0.0000  | 1.1626  |
| C2    | 0.0000  | 1.0920  | 0.3487  |
| C3    | 0.0000  | -1.0920 | 0.3487  |
| C4    | 0.0000  | 0.7169  | -0.9596 |
|  |  |  |  |
|---|---|---|---|
| C5 | 0.0000 | -0.7169 | -0.9596 |
| H6 | 0.0000 | 2.0473 | 0.8439 |
| H7 | 0.0000 | -2.0473 | 0.8439 |
| H8 | 0.0000 | 1.3509 | -1.8290 |
| H9 | 0.0000 | -1.3509 | -1.8290 |

**C₄H₅N (Pyrrole)**  1

|  |  |  |  |
|---|---|---|---|
| N1 | 0.0000 | 0.0000 | 1.1218 |
| H2 | 0.0000 | 0.0000 | 2.1178 |
| C3 | 0.0000 | 1.1209 | 0.3341 |
| C4 | 0.0000 | -1.1209 | 0.3341 |
| C5 | 0.0000 | 0.7076 | -0.9847 |
| C6 | 0.0000 | -0.7076 | -0.9847 |
| H7 | 0.0000 | 2.1084 | 0.7614 |
| H8 | 0.0000 | -2.1084 | 0.7614 |
| H9 | 0.0000 | 1.3566 | -1.8429 |
| H10 | 0.0000 | -1.3566 | -1.8429 |

**NO₂ (Nitrogen dioxide)**  2 1 1

|  |  |  |  |
|---|---|---|---|
| N1 | 0.0000 | 0.0000 | 0.0000 |
| O2 | 0.0000 | 1.0989 | 0.4653 |
| O3 | 0.0000 | -1.0989 | 0.4653 |

**SF₆ (Sulfur Hexafluoride)**  1

|  |  |  |  |
|---|---|---|---|
| S1 | 0.0000 | 0.0000 | 0.0000 |
| F2 | 0.0000 | 0.0000 | 1.5607 |
| F3 | 0.0000 | 1.5607 | 0.0000 |
| F4 | 1.5607 | 0.0000 | 0.0000 |
| F5 | 0.0000 | -1.5607 | 0.0000 |
| F6 | -1.5607 | 0.0000 | 0.0000 |
| F7 | 0.0000 | 0.0000 | -1.5607 |

**CFCl₃ (Trichloromonofluoromethane)**  1 2 2
| Compound | Formula | Bonding | C1 | C2 | C3 | C4 | C5 | Cl3 | Cl4 | Cl5 | F2 | F3 | F4 | F5 |
|----------|---------|---------|----|----|----|----|----|----|----|----|----|----|----|----|
| CF₃Cl (Methane, chlorotrifluoro-) | 1 2 2 | | | | | | | | | | | | | |
| C1 | 0.0000 | 0.0000 | 0.2472 |
| Cl2 | 0.0000 | 0.0000 | 1.5922 |
| F3 | 0.0000 | 1.6732 | -0.3101 |
| Cl4 | 1.4491 | -0.8366 | -0.3101 |
| Cl5 | -1.4491 | -0.8366 | -0.3101 |
| CF₃Cl | | | | | | | | | | | | | |
| C1 | 0.0000 | 0.0000 | -0.3471 |
| Cl2 | 0.0000 | 0.0000 | 1.4049 |
| F3 | 0.0000 | 1.2425 | -0.8074 |
| F4 | 1.0760 | -0.6212 | -0.8074 |
| F5 | -1.0760 | -0.6212 | -0.8074 |
| BF₃ (Bromotrifluoromethane) | 1 | | | | | | | | | | | | | |
| C1 | 0.0000 | 0.0000 | -0.8088 |
| Br2 | 0.0000 | 0.0000 | 1.1146 |
| F3 | 0.0000 | 1.2455 | -1.2651 |
| F4 | 1.0787 | -0.6228 | -1.2651 |
| F5 | -1.0787 | -0.6228 | -1.2651 |
| HCCF (Fluoroacetylene) | 1 2 2 | | | | | | | | | | | | | |
| C1 | 0.0000 | 0.0000 | -0.0942 |
| C2 | 0.0000 | 0.0000 | -1.2922 |
| F3 | 0.0000 | 0.0000 | 1.1848 |
| H4 | 0.0000 | 0.0000 | -2.3452 |
| HCCCN (Cyanoacetylene) | 1 2 2 | | | | | | | | | | | | | |
| N1 | 0.0000 | 0.0000 | 1.9018 |
| C2 | 0.0000 | 0.0000 | 0.7413 |
| C3 | 0.0000 | 0.0000 | -0.6351 |
| C4 | 0.0000 | 0.0000 | -1.8409 |
| H5 | 0.0000 | 0.0000 | -2.9033 |
| C₄N₂ (2-Butynedinitrile) | 1 2 2 | | | | | | | | | | | | | |
C1  0.0000  0.0000  2.5100
C2  0.0000  0.0000  3.7000
C3  0.0000  0.0000  1.1400
C4  0.0000  0.0000  5.0700
N5  0.0000  0.0000  0.0000
N6  0.0000  0.0000  6.2100

C2N2 (Cyanogen) 1 2 2
C1  0.0000  0.0000  0.6950
C2  0.0000  0.0000 -0.6950
N3  0.0000  0.0000  1.8450
N4  0.0000  0.0000 -1.8450

C3O2 (Carbon suboxide) 1 2 2
C1  0.0000  0.0000  0.0308
C2  0.0000  1.2509  0.0123
C3  0.0000 -1.2509  0.0123
O4  0.0000  2.3964 -0.0207
O5  0.0000 -2.3964 -0.0207

FCN (Cyanogen fluoride) 1 2 2
C1  0.0000  0.0000  0.0000
F2  0.0000  0.0000 -1.2620
N3  0.0000  0.0000  1.1590

C4H2 (Diacetylene) 1 2 2
C1  0.0000  0.0000  0.6890
C2  0.0000  0.0000 -0.6890
C3  0.0000  0.0000  1.8940
C4  0.0000  0.0000 -1.8940
H5  0.0000  0.0000  2.9520
H6  0.0000  0.0000 -2.9520

H2CS (Thioformaldehyde) 1 2 2
|        | x     | y     | z     |
|--------|-------|-------|-------|
| S1     | 0.0000| 0.0000| 0.5846|
| C2     | 0.0000| 0.0000| -1.0262|
| H3     | 0.0000| 0.9244| -1.5980|
| H4     | 0.0000| -0.9244| -1.5980|

**CHONH₂ (Formamide) 1 2 2**

|        | x     | y     | z     |
|--------|-------|-------|-------|
| C1     | 0.0000| 0.4165| 0.0000|
| O2     | 1.1942| 0.2217| 0.0000|
| N3     | -0.9373| -0.5551| 0.0000|
| H4     | -0.4299| 1.4182| 0.0000|
| H5     | -0.6608| -1.5171| 0.0000|
| H6     | -1.9020| -0.2881| 0.0000|

**CH₂CHCHO (Acrolein) 1**

|        | x     | y     | z     |
|--------|-------|-------|-------|
| C1     | -0.1496| -0.7423| 0.0000|
| C2     | 0.0000| 0.7200| 0.0000|
| C3     | 1.2291| 1.2662| 0.0000|
| O4     | -1.2313| -1.3044| 0.0000|
| H5     | 0.8007| -1.3120| 0.0000|
| H6     | -0.9066| 1.3142| 0.0000|
| H7     | 1.3716| 2.3428| 0.0000|
| H8     | 2.1072| 0.6273| 0.0000|

**CH₂CCl₂ (Ethene, 1,1-dichloro-) 1 2 2**

|        | x     | y     | z     |
|--------|-------|-------|-------|
| C1     | 0.0000| 0.0000| 1.7363|
| C2     | 0.0000| 0.0000| 0.4123|
| H3     | 0.0000| 0.9266| 2.2713|
| H4     | 0.0000| -0.9266| 2.2713|
| Cl5    | 0.0000| 1.4382| -0.5128|
| Cl6    | 0.0000| -1.4382| -0.5128|

**C₂HF₃ (Trifluoroethylene) 1 2 2**

|        | x     | y     | z     |
|--------|-------|-------|-------|
| C1     | 0.0000| 0.4436| 0.0000|
|    | C2      | F3      | F4      | F5      | H6      |
|----|---------|---------|---------|---------|---------|
|    | -0.7139 | 1.3153  | -0.5506 | -0.0873 | -1.8133 |
|    | -0.6916 | 0.4857  | 1.6388  | -1.8784 | -0.7269 |
|    | 0.0000  | 0.0000  | 0.0000  | 0.0000  | 0.0000  |

| CH₃CF₂ (Ethene, 1,1-difluoro) | 1 | 2 | 2 |
|-----------------------------|---|---|---|
| C1                          | 0.0000 | 0.0000 | 1.3851 |
| C2                          | 0.0000 | 0.0000 | 0.0701 |
| H3                          | 0.0000 | 0.9419 | 1.9094 |
| H4                          | 0.0000 | -0.9419 | 1.9094 |
| F5                          | 0.0000 | 1.0777 | -0.6972 |
| F6                          | 0.0000 | -1.0777 | -0.6972 |

| CH₃F (Methyl fluoride) | 1 | 2 | 2 |
|------------------------|---|---|---|
| C1                     | 0.0000 | 0.0000 | -0.6289 |
| F2                     | 0.0000 | 0.0000 | 0.7541 |
| H3                     | 0.0000 | 1.0201 | -1.0043 |
| H4                     | 0.8835 | -0.5101 | -1.0043 |
| H5                     | -0.8835 | -0.5101 | -1.0043 |

| CF₂Cl₂ (Difluorodichloromethane) | 1 | 2 | 2 |
|----------------------------------|---|---|---|
| C1                               | 0.0000 | 0.0000 | 0.3171 |
| F2                               | 0.0000 | 1.0758 | 1.1243 |
| F3                               | 0.0000 | -1.0758 | 1.1243 |
| Cl4                              | 1.4505 | 0.0000 | -0.6512 |
| Cl5                              | -1.4505 | 0.0000 | -0.6512 |

| SiF₂ (Silicon difluoride) | 1 | 2 | 2 |
|---------------------------|---|---|---|
| Si1                       | 0.0000 | 0.0000 | 0.5703 |
| F2                        | 0.0000 | 1.2249 | -0.4436 |
| F3                        | 0.0000 | -1.2249 | -0.4436 |
### TABLE XVII. Atomic energies (in kcal/mol) from the H atom to the Ar atom.

| Atom | Reference | $\omega$M05-D | M05-2X | $\omega$B97X-D |
|------|-----------|---------------|--------|---------------|
| H    | -313.76   | -311.52       | -313.31| -315.51       |
| He   | -1822.12  | -1822.11      | -1823.25| -1824.57     |
| Li   | -4692.56  | -4693.72      | -4694.37| -4699.80     |
| Be   | -9203.92  | -9198.97      | -9204.50| -9202.60     |
| B    | -15470.58 | -15466.17     | -15471.98| -15468.00   |
| C    | -23748.12 | -23746.17     | -23752.06| -23745.12   |
| N    | -34255.28 | -34254.32     | -34260.32| -34251.37   |
| O    | -47105.50 | -47107.44     | -47113.72| -47103.64   |
| F    | -62584.04 | -62587.59     | -62593.80| -62583.06   |
| Ne   | -80909.66 | -80910.31     | -80917.57| -80906.81   |
| Na   | -101816.42| -101814.09    | -101820.46| -101818.06 |
| Mg   | -125535.30| -125538.45    | -125549.12| -125538.97 |
| Al   | -152074.59| -152077.17    | -152084.44| -152078.77 |
| Si   | -181575.73| -181577.53    | -181581.20| -181577.86 |
| P    | -214143.51| -214141.04    | -214140.76| -214140.27 |
| S    | -249818.09| -249817.74    | -249815.58| -249817.21 |
| Cl   | -288747.57| -288747.04    | -288743.15| -288746.55 |
| Ar   | -331036.74| -331035.35    | -331028.07| -331036.25 |
| MSE  | 0.37      | -3.01         | -0.05  |
| MAE  | 2.02      | 5.10          | 2.51   |
| rms  | 2.42      | 6.31          | 2.96   |
### TABLE XVIII. Non-hydrogen transfer barrier heights (in kcal/mol) of the NHTBH38/04 set [63].

| Reactions                                      | $\Delta E_{ref}$ | $\omega$M05-D | M05-2X | $\omega$B97X-D |
|------------------------------------------------|------------------|----------------|--------|---------------|
| **Heavy-atom transfer reactions**               |                  |                |        |               |
| H + N$_2$O $\rightarrow$ OH + N$_2$             | $V_f$            | 18.14          | 16.52  | 18.82         | 17.47         |
|                                               | $V_r$            | 83.22          | 80.54  | 85.45         | 77.75         |
| H + FH $\rightarrow$ HF + H                    | $V_f$            | 42.18          | 38.34  | 41.16         | 40.56         |
|                                               | $V_r$            | 42.18          | 38.34  | 41.16         | 40.56         |
| H + CIH $\rightarrow$ HCl + H                   | $V_f$            | 18.00          | 17.83  | 19.64         | 18.19         |
|                                               | $V_r$            | 18.00          | 17.83  | 19.64         | 18.19         |
| H + FCH$_3$ $\rightarrow$ HF + CH$_3$           | $V_f$            | 30.38          | 28.76  | 31.70         | 30.02         |
|                                               | $V_r$            | 57.02          | 54.26  | 55.28         | 54.47         |
| H + F$_2$ $\rightarrow$ HF + F                  | $V_f$            | 2.27           | -0.07  | 2.90          | -0.60         |
|                                               | $V_r$            | 106.18         | 106.50 | 114.64        | 103.96        |
| CH$_3$ + FCl $\rightarrow$ CH$_3$F + Cl        | $V_f$            | 7.43           | 4.22   | 4.04          | 2.76          |
|                                               | $V_r$            | 60.17          | 57.63  | 59.94         | 56.55         |
| **Nucleophilic substitution reactions**         |                  |                |        |               |
| F$^-$ + CH$_3$F $\rightarrow$ FCH$_3$ + F$^-$  | $V_f$            | -0.34          | -1.79  | -1.93         | -1.37         |
|                                               | $V_r$            | -0.34          | -1.79  | -1.93         | -1.37         |
| F$^-$ $\cdots$ CH$_3$F $\rightarrow$ FCH$_3$ $\cdots$ F$^-$ | $V_f$ | 13.38          | 12.98  | 14.01         | 12.85         |
|                                               | $V_r$            | 13.38          | 12.98  | 14.01         | 12.85         |
| Cl$^-$ + CH$_3$Cl $\rightarrow$ ClCH$_3$ + Cl$^-$ | $V_f$ | 3.10           | 2.29   | 0.75          | 3.70          |
|                                               | $V_r$            | 3.10           | 2.29   | 0.75          | 3.70          |
| Cl$^-$ $\cdots$ CH$_3$Cl $\rightarrow$ ClCH$_3$ $\cdots$ Cl$^-$ | $V_f$ | 13.61          | 12.85  | 12.01         | 14.30         |
|                                               | $V_r$            | 13.61          | 12.85  | 12.01         | 14.30         |
| F$^-$ + CH$_3$Cl $\rightarrow$ FCH$_3$ + Cl$^-$ | $V_f$            | -12.54         | -14.38 | -15.89        | -13.58        |
|                                               | $V_r$            | 20.11          | 21.65  | 21.86         | 21.26         |
| F$^-$ $\cdots$ CH$_3$Cl $\rightarrow$ FCH$_3$ $\cdots$ Cl$^-$ | $V_f$ | 2.89           | 2.41   | 2.13          | 3.07          |
|                                               | $V_r$            | 29.62          | 31.11  | 31.97         | 30.50         |
| OH$^-$ + CH$_3$F $\rightarrow$ HOCH$_3$ + F$^-$ | $V_f$            | -2.78          | -3.96  | -4.22         | -3.31         |
|                                               | $V_r$            | 17.33          | 16.05  | 15.54         | 17.90         |
| OH$^-$ $\cdots$ CH$_3$F $\rightarrow$ HOCH$_3$ $\cdots$ F$^-$ | $V_f$ | 10.96          | 10.32  | 11.14         | 10.57         |
|                                               | $V_r$            | 47.20          | 49.33  | 48.84         | 49.20         |
| **Unimolecular and association reactions**      |                  |                |        |               |
| H + N$_2$ $\rightarrow$ HN$_2$                 | $V_f$            | 14.69          | 11.94  | 14.65         | 12.32         |
|                                               | $V_r$            | 10.72          | 12.01  | 13.07         | 13.40         |
| H + CO $\rightarrow$ HCO                       | $V_f$            | 3.17           | 2.91   | 4.96          | 3.37          |
|                                               | $V_r$            | 22.68          | 24.38  | 25.23         | 26.20         |
| H + C$_2$H$_4$ $\rightarrow$ C$_3$H$_2$       | $V_f$            | 1.72           | 2.46   | 3.68          | 3.03          |
|                                               | $V_r$            | 41.75          | 44.44  | 44.88         | 45.37         |
| CH$_3$ + C$_2$H$_4$ $\rightarrow$ CH$_3$C$_2$H$_2$ | $V_f$ | 6.85           | 4.13   | 4.09          | 4.57          |
|                                               | $V_r$            | 32.97          | 33.17  | 32.57         | 33.85         |
| HCN $\rightarrow$ HNC                         | $V_f$            | 48.16          | 44.78  | 46.45         | 46.42         |
|                                               | $V_r$            | 33.11          | 31.56  | 33.10         | 33.27         |
| **MSE**                                       | -0.94            | 0.13           | 0.45   | -0.45         |
| **MAE**                                       | 1.57             | 1.75           | 1.51   | 1.51          |
| **rms**                                       | 1.89             | 2.24           | 2.00   | 2.00          |
### TABLE XIX. Hydrogen transfer barrier heights (in kcal/mol) of the HTBH38/04 set [15, 63].

| Reactions | $\Delta E_{ref}$ | $\omega$M05-D | M05-2X | $\omega$B97X-D |
|-----------|----------------|--------------|-------|--------------|
| $\text{H} + \text{HCl} \rightarrow \text{H}_2 + \text{Cl}$ | $V^f$ | 5.7 | 3.61 | 4.82 | 4.08 |
| $\text{OH} + \text{H}_2 \rightarrow \text{H} + \text{H}_2\text{O}$ | $V^f$ | 5.1 | 1.94 | 4.61 | 2.22 |
| $\text{HCl} + \text{CH}_3 \rightarrow \text{Cl} + \text{CH}_4$ | $V^f$ | 15.3 | 13.35 | 16.07 | 13.54 |
| $\text{OH} + \text{CH}_3 \rightarrow \text{CH}_4 + \text{H}_2\text{O}$ | $V^f$ | 6.7 | 2.53 | 4.69 | 3.04 |
| $\text{OH} + \text{H}_2 \rightarrow \text{H} + \text{H}_2\text{O}$ | $V^f$ | 9.6 | 8.83 | 12.66 | 9.21 |
| $\text{H} + \text{H}_2 \rightarrow \text{H}_2 + \text{H}$ | $V^f$ | 3.2 | -0.14 | 2.67 | -0.02 |
| $\text{HCl} + \text{C}_2\text{H}_5 \rightarrow \text{Cl} + \text{C}_2\text{H}_4$ | $V^f$ | 12.7 | 9.73 | 12.41 | 9.69 |
| $\text{OH} + \text{C}_2\text{H}_6 \rightarrow \text{H}_2\text{O} + \text{C}_2\text{H}_5$ | $V^f$ | 3.4 | -0.28 | 2.19 | 0.17 |
| $\text{F} + \text{H}_2 \rightarrow \text{HF} + \text{H}$ | $V^f$ | 1.8 | -2.22 | 0.10 | -3.70 |
| $\text{O} + \text{CH}_4 \rightarrow \text{OH} + \text{CH}_3$ | $V^f$ | 13.7 | 8.85 | 10.62 | 9.20 |
| $\text{H} + \text{PH}_3 \rightarrow \text{PH}_2 + \text{H}_2$ | $V^f$ | 3.1 | 2.21 | 4.25 | 3.28 |
| $\text{H} + \text{HO} \rightarrow \text{H}_2 + \text{O}$ | $V^f$ | 10.7 | 7.90 | 10.38 | 8.84 |
| $\text{H} + \text{H}_2\text{S} \rightarrow \text{H}_2 + \text{HS}$ | $V^f$ | 13.1 | 8.15 | 11.16 | 8.89 |
| $\text{O} + \text{HCl} \rightarrow \text{OH} + \text{Cl}$ | $V^f$ | 8.1 | 4.39 | 5.50 | 4.67 |
| $\text{NH}_2 + \text{CH}_3 \rightarrow \text{CH}_4 + \text{NH}$ | $V^f$ | 8.0 | 5.41 | 7.10 | 5.65 |
| $\text{NH}_2 + \text{C}_2\text{H}_5 \rightarrow \text{C}_2\text{H}_6 + \text{NH}$ | $V^f$ | 9.8 | 4.95 | 7.01 | 5.47 |
| $\text{C}_2\text{H}_6 + \text{NH}_2 \rightarrow \text{NH}_3 + \text{C}_2\text{H}_5$ | $V^f$ | 22.4 | 18.17 | 20.33 | 18.41 |
| $\text{NH}_2 + \text{C}_2\text{H}_5 \rightarrow \text{C}_2\text{H}_6 + \text{NH}$ | $V^f$ | 7.5 | 7.09 | 8.56 | 7.26 |
| $\text{C}_2\text{H}_6 + \text{NH}_2 \rightarrow \text{NH}_3 + \text{C}_2\text{H}_5$ | $V^f$ | 18.3 | 15.22 | 17.68 | 15.69 |
| $\text{NH}_2 + \text{CH}_4 \rightarrow \text{CH}_3 + \text{NH}_3$ | $V^f$ | 14.5 | 10.81 | 12.71 | 11.28 |
| $s$–$\text{trans cis}$–$\text{C}_5\text{H}_8 \rightarrow \text{s}–\text{trans cis}$–$\text{C}_5\text{H}_8$ | $V^f$ | 38.4 | 37.23 | 39.06 | 39.07 |

**MSE** | -2.82 | -0.65 | -2.57 |
**MAE** | 2.83 | 1.51 | 2.70 |
**rms** | 3.16 | 1.83 | 3.10 |
TABLE XX. Interaction energies (in kcal/mol) for the S22 set with new reference values. The counterpoise corrections are used to reduce the basis set superposition errors. Monomer deformation energies are not included.

| Complex [Symmetry]                      | $\Delta E_{ref}$ | $\omega$M05-D | M05-2X | $\omega$B97X-D |
|----------------------------------------|------------------|----------------|--------|----------------|
| **Hydrogen bonded complexes**          |                  |                |        |                |
| (NH$_3$)$_2$[C$_{2h}$]                 | -3.133           | -3.00          | -3.12  | -3.08          |
| (H$_2$O)$_2$[C$_4$]                    | -4.989           | -4.89          | -5.08  | -4.97          |
| Formic acid dimer [C$_{2h}$]           | -18.753          | -18.98         | -19.41 | -19.28         |
| Formamide dimer [C$_{2h}$]             | -16.062          | -15.65         | -15.81 | -16.17         |
| Uracil dimer [C$_{2h}$]                | -20.641          | -19.90         | -19.64 | -20.43         |
| 2-pyridoxine-2-aminopyridine [C$_1$]   | -16.934          | -16.40         | -15.36 | -17.06         |
| Adenine-thymine WC [C$_4$]             | -16.660          | -15.87         | -14.84 | -16.46         |
| MSE                                    | 0.35             | 0.56           | -0.04  | 0.18           |
| MAE                                    | 0.42             | 0.77           | 0.18   |                |
| **Dispersion complexes**               |                  |                |        |                |
| (CH$_4$)$_2$[D$_{4d}$]                 | -0.527           | -0.65          | -0.51  | -0.57          |
| (C$_2$H$_4$)$_2$[D$_{2d}$]             | -1.472           | -1.70          | -1.42  | -1.79          |
| Benzene-CH$_4$[C$_3$]                  | -1.448           | -1.68          | -1.13  | -1.70          |
| Benzene dimer [C$_{2h}$]               | -2.654           | -3.55          | -1.38  | -3.16          |
| Pyrazine dimer [C$_2$]                 | -4.255           | -4.40          | -2.95  | -4.27          |
| Uracil dimer [C$_2$]                   | -9.805           | -9.83          | -8.32  | -9.79          |
| Indole-benzene [C$_1$]                 | -4.524           | -5.47          | -2.57  | -5.10          |
| Adenine-thymine stack [C$_1$]          | -11.730          | -12.00         | -9.40  | -11.86         |
| MSE                                    | 0.36             | 1.09           | -0.23  | 0.23           |
| MAE                                    | 0.36             | 1.09           | 0.23   |                |
| **Mixed complexes**                    |                  |                |        |                |
| Ethene-ethine [C$_{2v}$]               | -1.496           | -1.52          | -1.44  | -1.63          |
| Benzene-H2O [C$_4$]                    | -3.275           | -3.60          | -3.57  | -3.50          |
| Benzene-NH3 [C$_4$]                    | -2.312           | -2.54          | -2.23  | -2.53          |
| Benzene-HCN [C$_4$]                    | -4.541           | -4.76          | -4.90  | -4.79          |
| Benzene dimer [C$_{2v}$]               | -2.717           | -2.88          | -1.97  | -2.89          |
| Indole-benzene T-shape [C$_1$]         | -5.627           | -5.85          | -4.76  | -5.64          |
| Phenol dimer [C$_1$]                   | -7.097           | -6.89          | -6.03  | -6.99          |
| MSE                                    | 0.14             | 0.31           | -0.13  | 0.16           |
| MAE                                    | 0.20             | 0.50           | 0.16   |                |
| MSE                                    | -0.06            | 0.67           | -0.14  |                |
| MAE                                    | 0.33             | 0.80           | 0.19   |                |
| rms                                    | 0.42             | 1.06           | 0.25   |                |
TABLE XXI. Comparison of errors of different functionals for the reaction energies (in kcal/mol) of the 30 chemical reactions in the NHTBH38/04 and HTBH38/04 database \[15, 63\].

| Reactions | $\Delta E_{ref}$ | $\omega$M05-D | M05-2X | $\omega$B97X-D |
|-----------|------------------|--------------|--------|----------------|
| H + N$_2$O $\rightarrow$ OH + N$_2$ | -65.08 | -64.03 | -66.63 | -60.28 |
| H + FCH$_3$ $\rightarrow$ HF + CH$_3$ | -26.64 | -25.50 | -23.58 | -24.44 |
| H + F$_2$ $\rightarrow$ HF + F | -103.91 | -106.58 | -111.74 | -104.56 |
| CH$_3$ + FCl $\rightarrow$ CH$_3$F + Cl | -52.74 | -53.41 | -55.90 | -53.79 |
| F$^-$ + CH$_3$Cl $\rightarrow$ FCH$_3$ + Cl$^-$ | -32.65 | -36.03 | -37.75 | -34.84 |
| F$^-$ $\cdots$ CH$_3$Cl $\rightarrow$ FCH$_3$ $\cdots$ Cl$^-$ | -26.73 | -28.71 | -29.84 | -27.43 |
| OH$^-$ $\cdots$ CH$_3$F $\rightarrow$ HOCH$_3$ $\cdots$ F$^-$ | -36.24 | -39.01 | -37.70 | -38.63 |
| H + N$_2$ $\rightarrow$ HN$_2$ | 3.97 | 0.07 | 1.58 | -1.09 |
| H + CO $\rightarrow$ HCO | -19.51 | -21.47 | -20.27 | -22.83 |
| H + C$_2$H$_4$ $\rightarrow$ CH$_3$CH$_2$ | -40.03 | -41.98 | -41.20 | -42.35 |
| CH$_3$ + C$_2$H$_4$ $\rightarrow$ CH$_3$CH$_2$CH$_2$ | -26.12 | -29.04 | -28.48 | -29.28 |
| HCN $\rightarrow$ HNC | 15.05 | 13.22 | 13.35 | 13.16 |
| CH$_3$ + H$_2$ $\rightarrow$ H + CH$_4$ | -3.2 | -4.22 | -4.35 | -4.48 |
| OH + H$_2$ $\rightarrow$ H + H$_2$O | -16.1 | -16.75 | -17.29 | -16.55 |
| OH + CH$_4$ $\rightarrow$ CH$_3$ + H$_2$O | -12.9 | -12.53 | -12.94 | -12.07 |
| OH + NH$_3$ $\rightarrow$ H$_2$O + NH$_2$ | -9.5 | -9.87 | -9.75 | -9.71 |
| HCl + CH$_3$ $\rightarrow$ Cl + CH$_4$ | -6.2 | -5.29 | -5.47 | -4.98 |
| OH + C$_2$H$_6$ $\rightarrow$ H$_2$O + C$_2$H$_4$ | -16.5 | -17.16 | -17.06 | -16.40 |
| F + H$_2$ $\rightarrow$ HF + H | -31.6 | -33.00 | -33.29 | -32.71 |
| O + CH$_4$ $\rightarrow$ OH + CH$_3$ | 5.6 | 4.46 | 5.13 | 4.53 |
| H + PH$_3$ $\rightarrow$ PH$_2$ + H$_2$ | -20.1 | -21.25 | -21.37 | -20.18 |
| H + HO $\rightarrow$ H$_2$ + O | -2.4 | -0.25 | -0.78 | -0.05 |
| H + H$_2$S $\rightarrow$ H$_2$ + HS | -13.8 | -12.87 | -12.79 | -12.25 |
| O + HCl $\rightarrow$ OH + Cl | -0.6 | -0.83 | -0.34 | -0.45 |
| NH$_2$ + CH$_3$ $\rightarrow$ CH$_4$ + NH | -14.4 | -12.76 | -13.23 | -12.76 |
| NH$_2$ + C$_2$H$_5$ $\rightarrow$ C$_2$H$_6$ + NH | -10.8 | -8.13 | -9.11 | -8.43 |
| C$_2$H$_6$ + NH$_2$ $\rightarrow$ NH$_3$ + C$_2$H$_5$ | -7.0 | -7.29 | -7.31 | -6.69 |
| NH$_2$ + CH$_4$ $\rightarrow$ CH$_3$ + NH$_3$ | -3.3 | -2.66 | -3.20 | -2.37 |

MSE  
MAE  
rms
| Complex                        | $\Delta E_{ref}$ | $\omega$M05-D | M05-2X | $\omega$B97X-D |
|-------------------------------|------------------|---------------|--------|----------------|
| **Charge-transfer complexes** |                  |               |        |                |
| $\text{C}_2\text{H}_4 \cdots \text{F}_2$ | 1.06             | 0.79          | 1.00   | 0.78           |
| $\text{NH}_3 \cdots \text{F}_2$         | 1.81             | 1.41          | 1.44   | 1.50           |
| $\text{C}_2\text{H}_4 \cdots \text{CIF}$ | 3.81             | 3.82          | 4.51   | 3.66           |
| $\text{HCN} \cdots \text{CIF}$        | 4.86             | 4.21          | 4.72   | 4.21           |
| $\text{NH}_3 \cdots \text{Cl}_2$      | 4.88             | 4.61          | 5.02   | 4.81           |
| $\text{H}_2\text{O} \cdots \text{CIF}$ | 5.36             | 5.21          | 5.83   | 5.18           |
| $\text{NH}_3 \cdots \text{CIF}$      | 10.62            | 10.64         | 11.07  | 11.12          |
| MSE                           | -0.24            | 0.17          | -0.16  | 0.31           |
| MAE                           | 0.25             | 0.33          | 0.31   |                |
| **Dipole-dipole interaction complexes** |                  |               |        |                |
| $\text{H}_2\text{S} \cdots \text{H}_2\text{S}$ | 1.66             | 1.44          | 1.42   | 1.54           |
| $\text{HCl} \cdots \text{HCl}$       | 2.01             | 1.62          | 1.71   | 1.69           |
| $\text{H}_2\text{S} \cdots \text{HCl}$ | 3.35             | 3.26          | 3.23   | 3.38           |
| $\text{CH}_2\text{Cl} \cdots \text{HCl}$ | 3.55             | 3.08          | 3.24   | 3.17           |
| $\text{HCN} \cdots \text{CH}_3\text{SH}$ | 3.59             | 3.68          | 3.65   | 3.72           |
| $\text{CH}_3\text{SH} \cdots \text{HCl}$ | 4.16             | 4.82          | 4.84   | 4.87           |
| MSE                           | -0.07            | -0.04         | -0.04  | 0.01           |
| MAE                           | 0.32             | 0.28          | 0.28   |                |
| **Weak interaction complexes** |                  |               |        |                |
| $\text{He} \cdots \text{Ne}$        | 0.04             | -0.02         | 0.04   | 0.00           |
| $\text{He} \cdots \text{Ar}$        | 0.06             | -0.03         | 0.07   | 0.00           |
| $\text{Ne} \cdots \text{Ne}$        | -0.03            | -0.03         | 0.07   | -0.02          |
| $\text{He} \cdots \text{Ar}$        | 0.13             | -0.02         | 0.13   | -0.01          |
| $\text{CH}_4 \cdots \text{Ne}$      | 0.22             | 0.13          | 0.20   | 0.13           |
| $\text{CH}_4 \cdots \text{Ne}$      | 0.47             | 0.44          | 0.62   | 0.24           |
| $\text{CH}_4 \cdots \text{CH}_4$    | 0.51             | 0.68          | 0.51   | 0.60           |
| MSE                           | -0.05            | 0.02          | -0.08  | 0.00           |
| MAE                           | 0.10             | 0.03          | 0.11   |                |
| **Hydrogen-bonded DNA base pairs** |                  |               |        |                |
| $\text{G} \cdots \text{A HB}$       | -11.30           | -12.63        | -10.82 | -13.48         |
| $\text{C} \cdots \text{G WC}$       | -30.70           | -31.42        | -30.66 | -32.45         |
| $\text{G} \cdots \text{C WC}$       | -31.40           | -31.34        | -30.67 | -32.28         |
| MSE                           | -0.67            | 0.42          | -1.60  | 0.00           |
| MAE                           | 0.70             | 0.42          | 1.60   |                |
| **Interstrand base pairs**      |                  |               |        |                |
| $\text{G} \cdots \text{G IS}$      | -5.20            | -5.38         | -4.80  | -5.43          |
| $\text{G} \cdots \text{G IS}$      | 0.80             | 0.88          | 2.38   | 1.15           |
| $\text{C} \cdots \text{C IS}$      | 3.10             | 3.34          | 3.75   | 3.29           |
| MSE                           | 0.04             | 0.88          | 0.10   |                |
| MAE                           | 0.17             | 0.88          | 0.25   |                |
| **Stacked base pairs**         |                  |               |        |                |
| $\text{A} \cdots \text{G S}$      | -6.50            | -6.84         | -3.61  | -6.66          |
| $\text{C} \cdots \text{G S}$      | -12.40           | -11.09        | -8.57  | -10.83         |
| $\text{G} \cdots \text{C S}$      | -11.60           | -11.26        | -8.78  | -11.06         |
| MSE                           | 0.44             | 3.18          | 0.65   |                |
| MAE                           | 0.66             | 3.18          | 0.76   |                |
| MSE                           | -0.11            | 0.50          | -0.15  | 0.43           |
| MAE                           | 0.31             | 0.61          | 0.43   |                |