Cathodoluminescence Spectroscopy in Graded In$_x$Ga$_{1-x}$N

Xiaofang Zhao 1, Tao Wang 2,*, Bowen Sheng 3, Xiantong Zheng 3, Li Chen 2, Haihui Liu 1,*, Chao He 4, Jun Xu 2, Rui Zhu 2, and Xinqiang Wang 3

1 School of Materials Science and Engineering, Tiangong University, Tianjin 300387, China
2 Electron Microscopy Laboratory, School of Physics, Peking University, Beijing 100871, China
3 State Key Laboratory for Mesoscopic Physics and Frontiers Science Center for Nano-Optoelectronics, School of Physics, Peking University, Beijing 100871, China
4 Beijing Goldenscope Technology Co., Ltd., Beijing 100190, China
* Correspondence: cwwangtao@pku.edu.cn (T.W.); liuhaihui@tiangong.edu.cn (H.L.); zhurui@pku.edu.cn (R.Z.)

Abstract: InGaN materials are widely used in optoelectronic devices due to their excellent optical properties. Since the emission wavelength of the full-composition-graded In$_x$Ga$_{1-x}$N films perfectly matches the solar spectrum, providing a full-spectrum response, this makes them suitable for the manufacturing of high-efficiency optoelectronic devices. It is extremely important to study the optical properties of materials, but there are very few studies of the luminescence of full-composition-graded In$_x$Ga$_{1-x}$N ternary alloy. In this work, the optical properties of full-composition-graded In$_x$Ga$_{1-x}$N films are studied by cathodoluminescence (CL). The CL spectra with multiple luminescence peaks in the range of 365–1000 nm were acquired in the cross-sectional and plan-view directions. The CL spectroscopy studies were carried out inside and outside of microplates formed under the indium droplets on the InGaN surface, which found that the intensity of the light emission peaks inside and outside of microplates differed significantly. Additionally, the paired defects structure is studied by using the spectroscopic method. A detailed CL spectroscopy study paves the way for the growth and device optimization of high-quality, full-composition-graded In$_x$Ga$_{1-x}$N ternary alloy materials.

Keywords: full-composition-graded In$_x$Ga$_{1-x}$N films; cathodoluminescence; nitride semiconductor; paired defects

1. Introduction

III-nitride semiconductors and their alloys have received widespread attention due to their excellent optical and electrical properties. Among the nitride semiconductors, InGaN alloys are widely used in optoelectronic devices. In addition, by adjusting the composition of indium (In), the bandgap of InGaN alloys can be continuously adjusted from 0.64 eV to 3.4 eV, covering a continuous spectrum from near-infrared to ultra-violet (UV), and is an ideal material for devices emitting white light [1–3]. At the same time, InGaN material has a high optical absorption coefficient and a relatively high electron saturation drift rate. The emission wavelength of the full-composition-graded In$_x$Ga$_{1-x}$N material perfectly matches the solar spectrum, which provides a full-spectrum response and is suitable for the manufacture of high-efficiency photoelectric devices [4–6]. However, due to the poor crystal quality of InGaN materials, the efficiency of InGaN-based photoelectric device materials is severely limited [7–9]. The high balance vapor pressure and growth temperature difference between InN and GaN make it difficult to obtain high-quality InGaN materials, especially for growing full-composition InGaN ternary alloy. A thin film of full-composition-graded In$_x$Ga$_{1-x}$N ternary alloy has been successfully grown by molecular beam epitaxy (MBE), and several research groups have reported epitaxial growth of related full-composition ternary alloy (Miller [10] and Zheng [11]). To improve the quality of the InGaN ternary alloy, two-dimensional stepwise growth has been adopted [12], and epitaxial growth is
usually carried out under In-rich conditions and using growth temperature-controlled epitaxy [13]. Therefore, when growing a full-composition-graded In$_x$Ga$_{1-x}$N ternary alloy, In droplets were often formed on partial surfaces [14–18]. The full-composition-graded In$_x$Ga$_{1-x}$N ternary alloy can be applied in photoelectric devices and other fields. The study of the optical properties of In$_x$Ga$_{1-x}$N ternary alloy is extremely important, but reports on this are rare.

Here, we studied the optical properties of a full-composition-graded In$_x$Ga$_{1-x}$N ternary alloy film using cathodoluminescence (CL) measurements with a high spatial resolution and variable exciting electron beam. There are multiple luminescence peaks in the range of 365–1000 nm. Detailed CL spectroscopy was carried out inside and outside of the microplates, which formed under the indium drops after etching on the surface, and it was found that the emission intensity inside and outside of the microplates differs significantly.

2. Materials and Methods

The growth process of full-composition-graded In$_x$Ga$_{1-x}$N ternary alloy was reported [11]. Measurements of the high-angle annular dark-field scanning transmission electron microscopy (HAADF-STEM) were carried out using the aberration-corrected Thermo Fisher Scientific Titan Cubed Themis G2 transmission electron microscope operated at 300 kV. Morphology was characterized by ThermoFisher Quattro ESEM. CL spectra were obtained using Gatan Monochrome CL3+, a high-resolution CL probe with panchromatic and monochromatic reception at 300–1000 nm wavelengths, and Rainbow-CL system with a spectral detection range of 300–1000 nm.

3. Results

3.1. Composition and Structure of the Full-Composition-Graded In$_x$Ga$_{1-x}$N film

The full-composition-graded In$_x$Ga$_{1-x}$N ternary alloy gradually passes from GaN to InN, that is, x goes from 0 to 1 in the In$_x$Ga$_{1-x}$N ternary alloy. The scheme of the sample structure is shown in Figure 1a. A 450 nm-thick full-composition-graded In$_x$Ga$_{1-x}$N film was grown on GaN buffer layer by the MBE. The cross-sectional specimen was prepared by mechanical polishing and argon ion milling. Figure 1b is a HAADF-STEM image of an InGaN layer with multiple periodic quantum well (MQW) striking structures in the initial region of an In$_x$Ga$_{1-x}$N film. The high-In (light) and low-In (dark) In$_x$Ga$_{1-x}$N segments are composed of MQW-like structures that promote effective strain relaxation [19]. The formation of a periodic structure is associated with the relaxation of stress between InN and GaN with a large lattice mismatch (~11%) [20]. Most parts of the full-composition-graded In$_x$Ga$_{1-x}$N ternary alloy contain MQW-like structures, where with the decrease in growth temperature and the change in the growth mode, the atomic diffusion length decreases, and the periodical ordered structure disappears.

![Figure 1. (a) Schematic illustration of the full-composition-graded In$_x$Ga$_{1-x}$N. (b) HAADF-STEM image of the full-composition-graded In$_x$Ga$_{1-x}$N.](image-url)
3.2. Detailed Spectral Analysis of the Full-Composition-Graded $\text{In}_x\text{Ga}_{1-x}\text{N}$ film

To figure out the luminescence characteristics of quantum wells, CL measurements with high spatial and spectral resolution were used to accurately measure the luminescence of graded $\text{In}_x\text{Ga}_{1-x}\text{N}$ film. The luminescence of graded $\text{In}_x\text{Ga}_{1-x}\text{N}$ film in cross-sectional and plan-view were recorded at various accelerating voltages at room temperature. Figure 2a is a SEM image of a full-composition-graded $\text{In}_x\text{Ga}_{1-x}\text{N}$ film in a cross-sectional direction. As shown by the red dashed-line box, the 450-nm-thick layer at the surface is a graded $\text{In}_x\text{Ga}_{1-x}\text{N}$ layer.

The CL spectra of the cross-sectional samples derived from four randomly selected regions in the red frame in Figure 2a for a 5 kV electron beam, which are shown in Figure 2b. The CL spectra of each random region were obtained by continuous scanning of a $2.5 \times 0.5 \, \mu\text{m}^2$ area. One can see the edge emission of the GaN band at 365 nm and a broad peak related to deep-level emission at 565 nm (the so-called yellow band), which is most commonly attributed to defects associated with gallium vacancies ($V_{\text{Ga}}$) or defects associated with carbon [21,22]. Peaks between GaN and YL can be identified as the luminescence from the full-composition-graded $\text{In}_x\text{Ga}_{1-x}\text{N}$. As shown in Figure 2b, there are many irregular peaks, and broad peaks were found in the 400–800 nm range, proving the existence of luminescence in the entire visible spectral range.

In order to better understand all the luminescence peaks of a full-composition-graded $\text{In}_x\text{Ga}_{1-x}\text{N}$ ternary alloy film, CL spectra were collected with a 5 kV electron beam, and the wavelength distribution diagram of the luminescence peaks of the full-composition-graded $\text{In}_x\text{Ga}_{1-x}\text{N}$ ternary alloy film was extracted at room temperature (Figure 2c). The full-composition-graded $\text{In}_x\text{Ga}_{1-x}\text{N}$ ternary alloy film continuously emits light in the range from 365 nm to 800 nm. Theoretically, for the full-composition-graded $\text{In}_x\text{Ga}_{1-x}\text{N}$ ternary alloy film, the luminescence peak should be measured in the range of 365 nm–1850 nm. Due to the detection ability of our detector, the luminescence peak can only be seen in the range of 365–800 nm, which is further evidence that the full-composition-graded $\text{In}_x\text{Ga}_{1-x}\text{N}$ ternary alloy film has great potential to cover the entire solar spectrum. There are some differences in the distribution of luminescence peaks. The intensity of the peak is high in the range of 400 nm–480 nm, 510 nm–600 nm, and 700 nm–750 nm, indicating strong luminescence in these wavelength ranges.

The lateral distribution of optical properties of full-composition-graded $\text{In}_x\text{Ga}_{1-x}\text{N}$ ternary alloy was studied. As shown in Figure 3, different excitation voltages ranging from 5 kV to 15 kV were explored. Many microplates were spontaneously formed on the...
surface of full-composition-graded In$_x$Ga$_{1-x}$N films. Due to the degradation of crystal quality in the high-In composition region, the luminescence is weak at a low excitation voltage below 8 kV, and it is difficult to see a clear structure feature from CL images. With the increase in excitation voltage, the excitation depth of the electron beam can reach the low-In composition region. The crystal quality of these regions is high, so the CL signal and images are noticeable. However, since the In composition inside the microplates is higher than in other structures, the microplates could be observed more accurately at appropriate low voltages. The sizes of these In-rich microplates are not uniform, with the smallest microplate diameter being about 3 µm, while the largest microplate diameter is about 18 µm. The density of microplates is about $1.0 \times 10^5$ cm$^{-2}$, which is similar to the defects density of $1.23 \times 10^5$ cm$^{-2}$. We found that microplates have two different shapes: one is a typical “three-rings structure”, and the other is a “one-ring structure”. In addition, there is a different luminescence intensity in each microplate, which may be related to nonuniform In distribution. We also found that the defect structures always appeared in pairs near the microplates, that is, a circular defect structure with a diameter of about 3 µm and a dark spot structure with a diameter of about 5 µm. The luminescence intensity and In composition of the paired defects were also different. In order to verify the source of the paired defects, the CL spectrum analysis on the GaN buffer layer was conducted to exclude the possibility of a V-shaped defect in GaN. The density of the defects on the GaN buffer layer is approximately $7.9 \times 10^7$ cm$^{-2}$, which is much higher than the paired defects density of full-composition-graded InGaN and lower than the V-shaped defect density of GaN (see Supplementary Materials).

The luminescence characteristics of microplates and defect structures under different excitation voltages were further studied, as shown in Figure 4. There is a very clear CL spectral difference between the inside microplates (A–E) and the outside microplates (G). We conducted chemical wet etching for indium droplets. The indium droplets disappeared, leaving multiple “microplate” structures on the surface (see Supplementary Materials). The CL image shows that the overall luminescence intensity inside the microplates gradually decreases from the center (B) to the outer circle. Therefore, under the excitation voltage of 5 kV, the emission peaks (620 nm, 917 nm, and 976 nm) were observed in the spectra (Figure 4b).
Figure 3. CL images of full-composition-graded In$_x$Ga$_{1-x}$N film excited with electron beams ranging from 5 kV to 15 kV at room temperature.

The luminescence characteristics of microplates and defect structures under different excitation voltages were further studied, as shown in Figure 4. There is a very clear CL spectral difference between the inside microplates (A–E) and the outside microplates (G). We conducted chemical wet etching for indium droplets. The indium droplets disappeared, leaving multiple “microplate” structures on the surface (see Supplementary Materials). The CL image shows that the overall luminescence intensity inside the microplates gradually decreases from the center (B) to the outer circle. Therefore, under the excitation voltage of 5 kV, the emission peaks (620 nm, 917 nm, and 976 nm) were observed in the spectra (Figure 4b).

Figure 4. (a) SEM and CL images of full-composition-graded In$_x$Ga$_{1-x}$N film. (b, c) Their CL spectra of different structural positions (A–E, G) were obtained at 5 kV, 7 kV, and 9 kV beam voltages. The main CL peaks in Figure 4b, c have been indicated by arrows.

CL spectra of microplates outside (G) were obtained in Figure 4c, the luminescence peaks of microplates outside are mainly at 608 nm under the excitation voltage of 5 kV. Compared with the microplate (Figure 4b), the peak position of microplates outside was lower at 5 kV, and the composition of indium in microplates outside (Point G) is slightly lower than in microplates inside (Point B). Meanwhile, the CL luminescence intensity of microplates outside is the highest compared with other structures, and the crystal quality of microplates outside is the best, which is the main luminescence structure of the full-composition-graded In$_x$Ga$_{1-x}$N film. This indicated that the content of In in the inner microplate is higher than outer surface, an increase In content will lead to the deterioration of crystal quality [18]. Namely, as the In content increases, the quality of the crystal at B is worse than at G, so the quality of the microplates inside is worse than the microplates outside. This experimental result is also consistent with the corresponding theoretical analysis mentioned above. We believe that these differences can be associated with dislocations and uneven distribution of In composition in the film of the In$_x$Ga$_{1-x}$N ternary alloy.

Combined with CL images and CL spectra, we believe that the paired defects (F1 and F2) in Figure 5 could be caused by the following two factors: (1) Because the stable luminescence peak at various excitation voltages, the F1 point may be related to surface clustered penetration dislocations or other defects, which may stem from the GaN and InGaN interfaces or the InGaN layer, and the crystal quality is the worst. (2) During the growth process of full-composition-graded In$_x$Ga$_{1-x}$N film, the composition of In increased gradually with the growth process, while the crystal quality decreased, which may further generate partial short threading dislocations. In this process, the F2 point appears, and the peak position of CL spectra is mainly determined by the In composition. It was more direct to observe the correlation between the F1 point and F2 point for their crystal quality through CL mapping in Figure 5b. As a rule, the lattice and thermal mismatch between the epitaxial layer and substrate cause threading dislocations, in which nonradiative recombination centers reduce the quantum efficiency of light-emitting devices [17,23–25]. As the excitation voltage increases, the CL luminescence peaks of the F2 point move in the direction of the short wavelength. We found that the outline of the peak of the F2 point includes the F1 point in Figure 5c, which is related to the electron beam of interaction volume overlapping with the F1 and F2 points [26].
Figure 5. (a) SEM and CL images of the paired defects (F1 and F2). (b) CL mapping image of the paired defects at 10 kV beam voltages. The scanning area contains 50 × 38 pixels. (c) CL spectra of the paired defects at 5 kV, 7 kV, and 9 kV beam voltages. The main CL peaks have been indicated by arrows.

3.3. CL Mapping Observation of InGaN Microplates and Full-Composition-Graded In$_x$Ga$_{1−x}$N Film

CL measurements with high spectral and spatial resolution were performed to elucidate the lateral homogeneity and emission properties of InGaN at room temperature. Due to the inhomogeneous distribution of the In composition, some luminescence peaks can be concentrated in certain wavelength regions, which is related to fluctuations in the In composition during growth. Figure 6 shows a two-dimensional mapping image of InGaN with the CL wavelength ranging from 490 nm to 510 nm. The luminescence peaks of InGaN at 15 kV are mainly around 510 nm, while the luminescence peaks of paired defects are mainly around 503 nm. In addition, the luminescence wavelength of the two structures is not identical, with a difference in luminescence wavelength of about 7 nm.

Figure 6. Two-dimensional mapping of full-composition-graded In$_x$Ga$_{1−x}$N film under 15 kV excitation voltage with the wavelength range from 490 nm to 510 nm at room temperature.

There is a large lattice mismatch between the InGaN and the GaN buffer layer. The strain caused by lattice mismatch has a great influence on the growth process of InGaN,
especially the composition of indium. This phenomenon is called the composition-pulling effect [27], which makes it difficult to grow highly crystalline InGaN with a high In content on GaN. The incorporation of indium was inhibited by compressive strain but enhanced by tensile strain [28]. Thread dislocations penetrate the InGaN layer and reach the InGaN surface where the defects are formed. The formation of defects weakens the lattice deformation and the pulling effect of the composition [29], which is beneficial to the incorporation of indium, which leads to the composition of indium change—that is, the wavelength of the CL luminescence, which goes toward the long wavelength. The composition-pulling effect, strain, and defects decide the nonuniform In distribution.

The growth mechanism of InGaN microplates has been extensively studied [16,18,24,30–35], while the CL properties of full-composition-graded In_xGa_{1-x}N film are rarely reported, especially InGaN microplates. We found that the CL luminescence intensity of microplates inside was significantly weaker than microplates outside. This also indicates that the distribution of In components inside and outside of the microplates is not uniform. The composition of In in the In_xGa_{1-x}N microplates inside was higher than in InGaN microplates outside because more indium atoms were accumulated in the “ring”. Compositional fluctuations in the area of microplates are related to the process of growth microplates. In addition, we also found a sharp change in the light intensity at the edge of a single microplate, which may be due to the high efficiency of doping with absorbed indium atoms [18]. These results are also related to the surface energy of the In_xGa_{1-x}N alloy [36].

4. Conclusions

In this work, the luminescence characteristics of a full-composition-graded In_xGa_{1-x}N film are studied by SEM-CL. The results showed that visible luminescence peaks of the InGaN quantum structure were observed around 447 nm, 530 nm, 550 nm, 600 nm, 620 nm, 920 nm, and 976 nm. The full-composition-graded In_xGa_{1-x}N ternary alloy film continuously emits light in the range from 365 nm to 1000 nm, which shows that the In_xGa_{1-x}N materials have a promising spectral response with the solar spectrum. In addition, we analyzed the CL properties of InGaN microplates and paired defects on the surface of In_xGa_{1-x}N films. InGaN microplates can effectively control the CL luminescence characteristics of In_xGa_{1-x}N ternary alloy. These structures have a significant effect on the optical properties of In_xGa_{1-x}N films. The discovery of multi-wavelength luminescence peaks provides important ideas for the study of material growth and structure research of the full-composition-graded In_xGa_{1-x}N ternary alloy.

**Supplementary Materials:** The following supporting information can be downloaded at: https://www.mdpi.com/article/10.3390/nano12213719/s1, Section S1: CL spectra of full-composition-graded In_xGa_{1-x}N at low temperature; Section S2: CL spectrum of GaN buffer layer; Section S3: Excitation depth, In composition, and luminescence wavelength of full-composition-graded In_xGa_{1-x}N film at different excitation voltage; Section S4: In droplet structure on the full-composition-graded In_xGa_{1-x}N before etching. References [37,38] were cited in the Supplementary Materials.

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References

1. Lymperakis, L.; Schulz, T.; Freysoldt, C.; Anikeeva, M.; Chen, Z.; Zheng, X.; Shen, B.; Cheze, C.; Siekacz, M.; Wang, X.Q.; et al. Elastically frustrated rehybridization: Origin of chemical order and compositional limits in InGaN quantum wells. *Phys. Rev. Mater.* 2018, 2, 011601. [CrossRef]

2. Manzoor, H.U.; Zawawi, M.A.M.; Pahkuruddin, M.Z.; Ng, S.S.; Hassan, Z. High conversion and quantum efficiency indium-rich p-InGaN/p-InGaN/n-InGaN solar cell. *Phys. B Condens. Matter* 2020, 262, 413339. [CrossRef]

3. Massabau, F.C.P.; Horton, M.K.; Pearce, E.; Hammersley, S.; Chen, P.; Zielinski, M.S.; Weatherley, T.F.K.; Divitini, G.; Edwards, P.R.; Kappers, M.J.; et al. Optical and structural properties of dislocations in InGaN. *J. Appl. Phys.* 2019, 125, 165701. [CrossRef]

4. Guilleminoles, J.F.; El-Huni, W.; Migan, A.; Alamarguy, D.; Djebbour, Z. Modeling of InGaN/Si tandem cells: Comparison between 2-contacts/4-contacts. *EPJ Photovolta.* 2017, 8, 85502. [CrossRef]

5. Jiang, C.; Chen, Y.; Sun, J.; Jing, L.; Liu, M.; Liu, T.; Pan, Y.; Pu, X.; Ma, B.; Hu, W.; et al. Enhanced photocurrent in InGaN/GaN MQWs solar cells by coupling plasmonic with piezo-phototronic effect. *Nano Energy* 2019, 57, 300–306. [CrossRef]

6. Piralaee, M.; Asgari, A. The role of silver nanoparticles in performance of multi-quantum well double heterojunction InGaN/GaN solar cells. *Chem. Phys. Lett.* 2020, 754, 137500. [CrossRef]

7. der Maur, M.A.; Moses, G.; Gordon, J.M.; Huang, X.; Zhao, Y.; Katz, E.A. Temperature and intensity dependence of the open-circuit voltage of InGaN/GaN multi-quantum well solar cells. *Sol. Energy Mater. Sol. Cells* 2021, 230, 111253. [CrossRef]

8. Huang, X.; Chen, H.; Fu, H.; Baranowski, I.; Montes, J.; Yang, T.-H.; Fu, K.; Gunning, B.P.; Koleske, D.D.; Zhao, Y. Energy band engineering of InGaN/GaN multi-quantum-well solar cells via AlGaN electron- and hole-blocking layers. *Appl. Phys. Lett.* 2018, 113, 043501. [CrossRef]

9. Huang, X.; Li, W.; Fu, H.; Li, D.; Zhang, C.; Chen, H.; Fang, Y.; Fu, K.; DenBaars, S.P.; Nakamura, S.; et al. High-Temperature Polarization-Free III-Nitride Solar Cells with Self-Cooling Effects. *ACS Photon.* 2019, 6, 2096–2103. [CrossRef]

10. Miller, N.; Jones, R.E.; Yu, K.M.; Ager, J.W.; Liliental-Weber, Z.; Haller, E.E.; Walukiewicz, W.; Williamson, T.L.; Hoffbauer, M.A. Low-temperature grown compositionally graded InGaN films. *Phys. Status Solidi (C)* 2008, 5, 1866–1869. [CrossRef]

11. Zheng, X.T.; Wang, T.; Wang, P.; Sun, X.X.; Wang, D.; Chen, Z.Y.; Quach, P.; Wang, Y.X.; Yang, X.L.; Xu, F.J.; et al. Full-composition-grained InxGa1−xN films grown by molecular beam epitaxy. *Appl. Phys. Lett.* 2020, 117, 182101. [CrossRef]

12. Kurouchi, M.; Araki, T.; Naoi, H.; Yamaguchi, T.; Suzuki, A.; Nanishi, Y. Growth and properties of In-rich InGaN films grown on (0001) sapphire by RF-MBE. *Phys. Status Solidi (B)* 2004, 241, 2843–2848. [CrossRef]

13. Liu, S.T.; Wang, X.Q.; Chen, G.; Zhang, Y.W.; Feng, L.; Huang, C.C.; Xu, F.J.; Tang, N.; Sang, L.W.; Dey, S.; et al. Temperature-controlled epitaxy of InxGa1−xN films grown by molecular beam epitaxy. *J. Appl. Phys.* 2011, 110, 113514. [CrossRef]

14. Reyes, K.; Smereka, P.; Notthorn, D.; Millunchick, J.M.; Betti, S.; Somaschini, C.; Squintini, S.; Frigeri, C. Unified model of droplet epitaxy for compound semiconductor nanostructures: Experiments and theory. *Phys. Rev. B* 2013, 87, 165406. [CrossRef]

15. Mano, T.; Watanabe, K.; Tsukamoto, S.; Fujiioka, H.; Oshima, M.; Koguchi, N. Fabrication of InGaaS quantum dots on GaAs(0 0 1) by droplet epitaxy. *J. Cryst. Growth* 2000, 209, 504–513. [CrossRef]

16. Wu, J.; Wang, Z.M.; Li, A.Z.; Benamara, M.; Li, S.; Salamo, G.J. Nanoscale footprints of self-running gallium droplets on GaAs surface. *Plos ONE* 2011, 6, e20765. [CrossRef]

17. Zheng, X.; Huang, W.; Liang, H.; Wang, P.; Liu, Y.; Chen, Z.; Liang, P.; Li, M.; Zhang, J.; Chen, Y.; et al. Investigation of InGaN Layer Grown Under In-Rich Condition by Reflectance Difference Spectroscopy Microscope. *J. Nanosci. Nanotechnol.* 2018, 18, 7468–7472. [CrossRef]

18. Zheng, X.; Liang, H.; Wang, P.; Sun, X.; Chen, Z.; Wang, T.; Sheng, B.; Wang, Y.; Chen, L.; Wang, D.; et al. Effect of island droplets on growth of InGaN film by molecular beam epitaxy. *Superlattices Microstruct.* 2018, 113, 650–656. [CrossRef]

19. Wang, T.; Liu, S.; Zheng, X.; Wang, P.; Wang, D.; Chen, Z.; Wei, J.; Rong, X.; Tao, R.; Guo, S.; et al. Microstructure and dislocation evolution in composition gradient AlGaN grown by MOCVD. *Superlattices Microstruct.* 2021, 152, 106842. [CrossRef]

20. Wu, Z.H.; Kawai, Y.; Fang, Y.Y.; Chen, C.Q.; Kondo, H.; Hori, M.; Honda, Y.; Yamaguchi, M.; Amano, H. Spontaneous formation of highly regular superlattice structure in InGaN epilayers grown by molecular beam epitaxy. *Appl. Phys. Lett.* 2011, 98, 141905. [CrossRef]

21. Castaldini, A.; Cavallini, A.; Polenta, L. Yellow and green bands in GaN by resolved spectral photocconductivity. *Appl. Phys. Lett.* 2005, 87, 122105. [CrossRef]

22. Reschchikov, M.A.; Morkoç, H. Luminescence properties of defects in GaN. *J. Appl. Phys.* 2005, 97, 061301. [CrossRef]

23. Dai, Q.; Schubert, M.F.; Kim, M.H.; Kim, J.K.; Schubert, E.F.; Koleske, D.D.; Crawford, M.H.; Lee, S.R.; Fischer, A.J.; Thaler, G.; et al. Internal quantum efficiency and nonradiative recombination coefficient of GaN/InN/GaN multiple quantum wells with different dislocation densities. *Appl. Phys. Lett.* 2009, 94, 111109. [CrossRef]

24. Dai, Y.; Dabrowski, M.; Petek, H. Optical field tuning of localized plasmon modes in Ag microcrystals at the nanofemtosecond scale. *J. Chem. Phys.* 2020, 152, 054201. [CrossRef] [PubMed]

25. Kim, J.; Cho, Y.H.; Ko, D.S.; Li, X.S.; Won, J.Y.; Lee, E.; Park, S.H.; Kim, J.Y.; Kim, S. Influence of V-pits on the efficiency droop in InGaAs/GaAs quantum wells. *Opt. Express* 2014, 22, A857–A866. [CrossRef]

26. Narvaez, A.C.; Weppelman, I.G.C.; Moerland, R.J.; Liv, N.; Zonnevylle, A.C.; Kruit, P.; Hoogenboom, J.P. Cathodoluminescence Microscopy of nanostructures on substrates. *Opt. Express* 2013, 21, 29968–29978. [CrossRef] [PubMed]
27. Stringfellow, G.B. Microstructures produced during the epitaxial growth of InGaN alloys. *J. Cryst. Growth* 2010, 312, 735–749. [CrossRef]

28. Inatomi, Y.; Kangawa, Y.; Ito, T.; Suski, T.; Kumagai, Y.; Kakimoto, K.; Koukitu, A. Theoretical study of the composition pulling effect in InGaN metalorganic vapor-phase epitaxy growth. *Jpn. J. Appl. Phys.* 2017, 56, 078003. [CrossRef]

29. Hiramatsu, K.; Kawaguchi, Y.; Shimizu, M.; Sawaki, N.; Zheleva, T.; Davis, R.F.; Tsuda, H.; Taki, W.; Kuwano, N.; Oki, K. The Composition Pulling Effect in MOVPE Grown InGaN on GaN and AlGaN and its TEM Characterization. *MRS Internet J. Nitride Semicond. Res.* 2014, 2, 11. [CrossRef]

30. Kruse, C.; Einfeldt, S.; Böttcher, T.; Hommel, D.; Rudloff, D.; Christen, J. Spatially modified layer properties related to the formation of gallium droplets on GaN (0001) surfaces during plasma-assisted molecular-beam epitaxy. *Appl. Phys. Lett.* 2001, 78, 3827–3829. [CrossRef]

31. Gurioli, M.; Wang, Z.; Rastelli, A.; Kuroda, T.; Sanguinetti, S. Droplet epitaxy of semiconductor nanostructures for quantum photonic devices. *Nat. Mater.* 2019, 18, 799–810. [CrossRef] [PubMed]

32. Horton, M.K.; Rhode, S.; Sahonta, S.L.; Kappers, M.J.; Haigh, S.J.; Pennycook, T.J.; Humphreys, C.J.; Dusane, R.O.; Moram, M.A. Segregation of In to dislocations in InGaN. *Nano Lett.* 2015, 15, 923–930. [CrossRef]

33. Azadmand, M.; Vichi, S.; Betti, S.; Christina, D.; Bonera, E.; Acciarri, M.; Fedorov, A.; Tsukamoto, S.; Nötzel, R.; Sanguinetti, S. Metal Droplet Effects on the Composition of Ternary Nitrides. *arXiv* 2019, arXiv:1907.06939.

34. Nemcsics, A. Quantum Dots Prepared by Droplet Epitaxial Method. In *Quantum Dots—Theory and Applications*; Scitus Academics LLC: Wilmington, DE, USA, 2015; p. 48775. [CrossRef]

35. Tong, C.Z.; Yoon, S.F. Investigation of the fabrication mechanism of self-assembled GaAs quantum rings grown by droplet epitaxy. *Nanotechnology* 2008, 19, 365604. [CrossRef]

36. Romano, J.E.N.L.T. Surface energetics, pit formation, and chemical ordering in InGaN alloys. *Appl. Phys. Lett.* 1999, 74, 2319–2321. [CrossRef]

37. Trager-Cowan, C.; Middleton, P.G.; Mohammed, A.; O’Donnell, K.P.; Van der Stricht, W.; Moerman, I.; Demeeester, P. Probing the Indium Mole Fraction in an InGaN Epilayer by Depth Resolved Cathodoluminescence. *MRS Online Proc. Libr.* 1997, 482, 738–741. [CrossRef]

38. McCluskey, M.D.; Van de Walle, C.G.; Romano, L.T.; Krusor, B.S.; Johnson, N.M. Effect of composition on the band gap of strained InxGa1−xN alloys. *J. Appl. Phys.* 2003, 93, 4340–4342. [CrossRef]