Strategies to Ensure Accurate Calculation of Parameters of the VO₂ Response Profile During Heavy Intensity Cycle Ergometer Exercise

David Wilfred Hill¹ *

¹Department of Kinesiology, Health Promotion, and Recreation, University of North Texas, Denton, United States
*Corresponding author: Department of Kinesiology, Health Promotion, and Recreation, University of North Texas, 1155 Union Circle #310769, Denton, United States. Tel: +1-4697863769, Email: david.hill@unt.edu

Received 2019 September 16; Accepted 2019 September 28.

Abstract

**Background:** The parameters of the VO₂ response profile are obtained by fitting breath-by-breath VO₂ data from an exercise test to an appropriate mathematical model. Several strategies have been recommended to ensure, or at least improve, the accuracy of the values.

**Objectives:** The purpose of this study was to evaluate two strategies to enhance the accuracy of parameter estimates that describe the two-component VO₂ response during heavy intensity exercise. The first was to use data from a number of tests rather than just one. The second was to ‘smooth’ the data, using three-breath, five-breath, or seven-breath rolling averages of the breath-by-breath VO₂ data prior to fitting the data to the two-component model.

**Methods:** Twenty participants (eight women and twelve men) performed six 6-min heavy-intensity (midway between the ventilatory threshold and VO₂max) cycle ergometer tests. Breath-by-breath data and smoothed data from each test were fit to a two-component model. The parameter estimates from the first test, and the average of the values from the first two, first three, first four, first five, and all six tests were compared against the criterion value, which was the average of all six values obtained using five-breath averages.

**Results:** Modeling five-breath averages of data from the first test generated values for the parameters that were closely related to the criterion values. Modeling data from two or three tests improved the accuracy slightly, but improvements were small, and negligible when more than three tests were included.

**Conclusions:** Depending upon the accuracy required, that is depending upon how close each and every participant’s value must be to his or her ‘true’ value, smoothed data from one or two tests is sufficient to calculate the values that describe the two-parameter VO₂ response profile in heavy intensity cycling exercise.

**Keywords:** Kinetics, Heavy Intensity, Modeling, Cycling, Slow Component

1. Background

The pulmonary VO₂ response profile in exercise reflects the underlying metabolic activity in the muscles (1, 2). In moderate intensity exercise, work rates below the lactate threshold, the metabolic response is mirrored by the mono-exponential increase in VO₂ leading to rapid attainment of a steady state (1). For exercise in the heavy domain, which comprises work rates above the lactate threshold and up to critical power or critical speed, the asymptote of the relationship between time to exhaustion and work rate or speed (3-5), the rate of lactate production is said to be balanced by the rate of removal, so the blood lactate concentration will increase in the first few minutes and then decrease gradually or stay steady (6); this metabolic profile is reflected in the two-phase VO₂ response, which features (i) a primary phase or fast response followed by (ii) a slow phase or slow component, which emerges after ~2 min of exercise and leads to a steady-state VO₂ (7). In severe exercise, there is two-phase VO₂ response and, if exercise is continued long enough, the slow component will bring the VO₂ to VO₂max (7).

Characteristics of the VO₂ response profile—or parameters of the kinetics of the VO₂ response—are determined using a three-phase process: data collection, data processing, and data fitting (8). Since the advent of automated gas analysis systems that provide VO₂ data on a breath-by-breath (B×B) basis, these are the systems of choice for collecting data. The second phase, data processing, involves treating the data to ensure that parameters are estimated with the greatest precision and accuracy during the final
phase. This data processing aims to improve the signal (the underlying responses) to noise (breath to breath variability) ratio (1, 9, 10). The final phase is data fitting, the mathematical process of fitting the breath-by-breath VO\textsubscript{2} data to an appropriate mathematical model using iterative nonlinear regression procedures on any number of readily available statistical or graphing packages to identify what the values of the parameters are the best describe how closely the actual data fit the model. Using these packages, parameter estimates are generated, each with an associated SEE, which describes the precision of the estimates.

The focus of the present study is on the second phase, data processing. We assume that data are collected carefully on a B × B basis, using calibrated equipment, under reasonable environmental conditions, from participants who are properly prepared and motivated. We assume that an appropriate statistical analysis package is available and that an acceptable model has been selected.

Two approaches have been taken in order to improve the precision, and ensure the accuracy, of parameter estimates. First, the breath-by-breath data have been ‘smoothed’—for example, by using interpolation to generate second-by-second values or by generating three-breath (3-B), five-breath (5-B), or seven-breath (7-B) (etc.) rolling averages—prior to performing the iterative progression (9). Second, data have been collected from several identical exercise tests—the parameter estimates generated by mathematical modeling of the data from each test can been combined (averaged) or the data from the tests can been combined prior to mathematical modeling (8, 9). While it may be inherently obvious that smoothing data or replicating the exercise tests would improve the precision of parameter estimates, relatively little research has sought to determine the optimal treatment of exercise data to ensure the accuracy of the parameter values (9).

2. Objectives

The objective of this study was to evaluate the impact of these two strategies to improve the accuracy of the descriptors of the VO\textsubscript{2} response profile during heavy intensity cycle ergometer exercise. Twenty participants performed six identical exercise tests. B × B data from each test, as well as rolling 3-B, 5-B, and 7-B averages, were fitted to a two-component (primary + slow) model. Parameter estimates from the combinations of number of tests used (one to six) and the methods of smoothing (none, 3-B, 5-B, and 7-B rolling averages) were compared against a criterion value. The purpose of this study was to identify the optimal smoothing method and the minimum number of tests necessary to ensure accurate estimation of the parameters of the VO\textsubscript{2} response in heavy intensity exercise.

3. Methods

3.1. Participants

The study procedures were approved by the Institutional Review Board for the Protection of Human Subjects in Research at the university prior to any recruitment of participants. The study was conducted in accordance with the latest Declaration of Helsinki (11). Eight women (mean ± SD: age 22 ± 1 y, height 167 ± 9 cm, weight 66 ± 11 kg, VO\textsubscript{2max} 39 ± 6 mL.kg\textsuperscript{−1}.min\textsuperscript{−1} and twelve men (23 ± 2 y, 182 ± 8 cm, 79 ± 12 kg, 43 ± 5 mL.kg\textsuperscript{−1}.min\textsuperscript{−1}) volunteered to participate and provided informed consent. These 20 participants were involved in recreational sport or fitness activities, but not organized sport activities. They were all familiar with exercise testing procedures and for breathing through a mouthpiece. They verified that they did not change their exercise routines, diet, or sleep habits over the course of the study.

3.2. Overview

Participants performed an incremental test for determination of their VO\textsubscript{2max} and the VO\textsubscript{2} at the ventilatory threshold. Then they performed a series of six 6-min tests at a work rate individually selected so that the oxygen demand would be midway between VO\textsubscript{2max} and the VO\textsubscript{2} at the ventilatory threshold. The testing sessions were separated by at least 24 hours and were scheduled at the same time of day for each participant to avoid the confounding effects of time of day that we have reported on responses associated with the ventilatory threshold (12) and in severe intensity VO\textsubscript{2} kinetics (13); the work rates used in the present study lay between the ventilatory threshold and the lower boundary of the severe intensity domain. Tests were performed under similar conditions in a temperature-controlled laboratory (20°C to 22°C; ~50% relative humidity), with no distractions. Data collection was completed in a three-week period. Participants were instructed to sleep at least six hours the night before each test; not to exercise and not to ingest carbonated beverages, caffeine, or alcohol for 12 hours before each test; and not to eat a heavy meal in the three hours before each test. Actual dietary intake was at each participant’s discretion and was not recorded. They were tested only if they verified that they had adhered to all these instructions.
3.3. Incremental Tests to Determine \( VO_{2\max} \)

The incremental tests were performed on a Monark Ergomedic 828E (Varberg, Sweden) cycle ergometer, with pedaling cadence of \( \sim 80 \) revolutions per min (rev/min). A digital readout of the cadence was visible during the tests. The tests began with three minutes of baseline data collection during seated rest. The initial work rates were 40 W for women and 80 W for men. Work rate was abruptly increased 20 W each minute.

Throughout each test, expired gases were analyzed using a MedGraphics (St. Paul, Minnesota, USA) Express metabolic cart. The cart was calibrated before each test according to the manufacturer’s instructions. Breath-by-breath \( VO_{2} \) data were reduced to serial 15-s averages. Tests were terminated when the participant allowed the cadence to drop below 70 rev.min\(^{-1} \) for five seconds, despite strong verbal encouragement. \( VO_{2\max} \) was determined as the highest average of adjacent 15-s averages. The ventilatory threshold was identified as described by Wasserman and colleagues (14).

3.4. Constant Power Heavy Intensity Tests

Tests were performed using the same Monark ergometer as for the incremental tests, and during each test, expired gases were analyzed using the same MedGraphics metabolic cart. The tests began with three minutes of baseline data collection during seated rest. After the rest, the participant began pedaling and rapidly brought the pedaling cadence up to 80 (rev.min\(^{-1} \)) as the resistance was abruptly increased to provide the work rate that had been individually pre-determined by the primary investigator.

3.5. \( VO_{2} \) Kinetics in the Constant Power Tests

For each individual, for each test, data from the first 20 s of exercise were removed (8) and the remaining B \( \times \) B, 3-B, 5-B, or 7-B data points were fit to the following model (1) using iterative regression procedures in KaleidaGraph 4.5 software (Reading, PA USA) (Equation 1):

\[
VO_{2}(t) = VO_{2baseline} + A_{primary} \times \left(1 - e^{-\left(\frac{t - TD_{primary}}{\tau_{primary}}\right)}\right) + A_{slow} \left(1 - e^{-\left(\frac{t - TD_{slow}}{\tau_{slow}}\right)}\right)
\]

\( VO_{2baseline} \) is the steady state \( VO_{2} \) at the end of the three minutes of seated rest prior to exercise, \( A_{primary} \) and \( A_{slow} \) are the projected increases in \( VO_{2} \) due to the primary and slow component responses, \( TD_{primary} \) and \( TD_{slow} \) are the time delays preceding the two responses, and \( \tau_{primary} \) and \( \tau_{slow} \) are the time constants of the two responses.

The mean response time (\( MRT_{primary} \)) represents the time from the start of exercise until the \( VO_{2} \) has increased 63% of the \( A_{primary} \). It is calculated as the sum of \( TD_{primary} \) and \( \tau_{primary} \) and tends to be more stable and reliable than either of the parameters which it comprises. \( MRT_{primary} \) was used as a supplementary variable to describe the primary phase of the \( VO_{2} \) response.

The actual increase in \( VO_{2} \) due to the slow component, \( A'_{slow} \), was calculated as (Equation 2):

\[
A_{slow}' = A_{slow} \times \left(1 - e^{-\left(\frac{t_{exhaustion} - TD_{slow}}{\tau_{slow}}\right)}\right)
\]

\( A_{slow}' \) and \( TD_{slow} \) were used to describe the characteristics of the slow component in all tests.

3.6. Statistical Analyses

Descriptive characteristics of participants were calculated separately for women and men. For all other analyses, data were collapsed across the sexes. Sample size was 20.

First, to identify which smoothing method would be selected to provide the criterion measure for each parameter, the SEE of each parameter that was directly generated using the iterative regression procedure in KaleidaGraph (\( TD_{primary} \), \( \tau_{primary} \), \( A_{primary} \), and \( TD_{slow} \)) were compared using a two-way (type of smoothing [B \( \times \) B, 3-B, 5-B, 7-B] \( \times \) test number [first, second, third, fourth, fifth, sixth]) repeated-measures analysis of variance (ANOVA) in SPSS V22 (SPSS, Armonk, NY, USA). Two other descriptors of the \( VO_{2} \) response profile, \( MRT_{primary} \) and \( A_{slow}' \), were not included because they are calculated values, and not directly generated by KaleidaGraph. Data were tested for sphericity using Mauchly’s test of sphericity and, if assumptions were violated, results were interpreted using a Greenhouse-Geisser correction. Significance was set at \( P < 0.05 \). The post hoc comparisons of SEE were performed using paired-means \( t \) tests with a fixed level of significance (\( P < 0.05 \)) rather than correcting the \( P \)-level because of multiple comparisons; given that these comparisons were a tool to identify the criterion measure and any difference was considered meaningful. Data are presented as mean \( \pm \) SD.

Second, the optimal smoothing method and the minimum number of tests necessary to ensure accurate estimation of the parameters of the \( VO_{2} \) response in heavy intensity exercise, six values for each parameter (\( TD_{primary} \), \( \tau_{primary} \), \( MRT_{primary} \), \( A_{primary} \), \( TD_{slow} \), and \( A_{slow}' \)), and for the SEE associated with the four parameters that were directly...
generated by KaleidaGraph) obtained using each smoothing method were calculated. The first of the six values was simply the value from the first test, the second was the average of the values from the first and second tests, the third was the average of the values from the first three tests, etc. These values were compared using a two-way (type of smoothing $[B \times B, 3-B, 5-B, 7-B] \times$ number of tests used to calculate the value $[1, 2, 3, 4, 5, 6]$) repeated-measures ANOVA. In addition, correlations between each value and the criterion measure were calculated.

Finally, a Bland-Altman plot (15) was created for each comparison. Arguably, use of a Bland-Altman analysis is preferred when the task is to identify methods that produce the same answer (in this case, to identify methods that produce an answer that is the same as the criterion), as opposed to identifying values or methods that are different. As proposed by Krouwer (16), criterion values were on the x-axis and differences between values and the criterion were on the y-axis. Aside from the fact that 23 Bland-Altman plots were needed to assess the agreement between the various means and the criterion measure for each variable, one challenge of using Bland-Altman plots was that levels of agreement (defined by the 95% confidence interval around the mean difference for each comparison) were different for each comparison, even for comparisons for the same variable. This meant, for example, that for any given parameter, some types of smoothing faced stricter limits of agreement than others. In addition, Bland and Altman (15) noted that the levels of agreement that they propose (95% confidence interval around the mean difference) may be unacceptably large in some situations, such as clinical testing, and this was the case in the present study: the 95% confidence interval in many cases was simply too broad, as the SEE of the criterion measure. We estimate that these SEE of the criterion measure. We assumed that the average of the values from the six tests tended to be smallest for 5-B averages, as well (these results not provided, but can be inferred from data in Tables 1-4). We assumed that the average value from all six tests would be most representative of the ‘true’ or criterion value.

Based on the mathematically smaller SEE associated with parameters generated using 5-B smoothing, this method was chosen to identify the criterion values for all parameters. We note that the coefficient of variation among the values from the six tests tended to be smallest for 5-B averages, as well (these results not provided, but can be inferred from data in Tables 1-4). We assumed that the average value from all six tests would be most representative of the ‘true’ or criterion value.

Mean values for the parameter that were obtained using the 24 combinations of kind-of-smoothing ($B \times B$, $3-B$, $5-B$, $7-B$) and number-of-tests used to calculate the values (1 to 6) are presented in Tables 1-5. Results of the two-way ANOVAs that were used to investigate the effects of smoothing and number of tests revealed no significant main or interaction effects. Thus, we cannot argue that there were any differences among the reported values, regardless of the type of smoothing or the number of tests used to calculate the values. Similarly, the results of the correlational analyses, which are also presented in the tables, showed that values from almost all combinations of type of smoothing and number of tests used were strongly correlated with the criterion 5-B six test values. Because of space limitations, results for the MRT$_{primary}$, which was calculated as the sum of TD$_{primary}$ and tau$_{primary}$, are not provided in tabular form. Variability in MRT$_{primary}$ is much less than in either parameter individually; thus, the accuracy of MRT$_{primary}$ generated with data from one test was acceptable, regardless of how the data were smoothed.

Two hundred and seventy-six Bland-Altman plots were constructed (6 variables $\times$ 2 levels of agreement $\times$ 23 comparisons). Because of space restrictions, the plots are not reproduced here. The important results from these plots

4. Results

Results of the two-way ANOVA that was used to identify which smoothing method would be selected to provide the criterion measure for each parameter revealed a significant effect of type of smoothing ($P < 0.05$) for three of the six parameters generated with the parameter estimates that were directly generated using KaleidaGraph (tau$_{primary}$, A$_{primary}$, and TD$_{slow}$, but not TD$_{primary}$). The mean values associated with the main effects are presented in the farthest right column of Tables 1-4 and the results of the post hoc t tests are provided below, with differences significant at the 0.05 level:

- SEE TD$_{primary}$, $B \times B = 7-B = 3-B = 5-B$
- SEE tau$_{primary}$, $B \times B > 3-B = 7-B > 5-B$
- SEE A$_{primary}$, $B \times B > 3-B = 7-B = 5-B$
- SEE TD$_{slow}$, $B \times B > 3-B > 5-B = 7-B$

Based on the mathematically smaller SEE associated with parameters generated using 5-B smoothing, this method was chosen to identify the criterion values for all parameters. We note that the coefficient of variation among the values from the six tests tended to be smallest for 5-B averages, as well (these results not provided, but can be inferred from data in Tables 1-4). We assumed that the average value from all six tests would be most representative of the ‘true’ or criterion value.

4. Results
Table 1. Estimates of $TD_{primary}$ (with Units of s) Generated Using the Results from the First Test, the First Two Tests, the First Three Tests, the First Four Tests, the First Five Tests, and All Six Tests$^a$, $^b$

| Type of Smoothing | Number of Values Averaged (Number of Tests Included in Calculation) |
|-------------------|---------------------------------------------------------------|
|                   | 1                  | 2                  | 3                  | 4                  | 5                  | 6                  |
| B × B             |                    |                    |                    |                    |                    |                    |
| Mean              | 6 ± 9              | 7 ± 7              | 7 ± 8              | 8 ± 7$^c$           | 9 ± 8$^b$          | 10 ± 8$^b$         |
| SEE               | 8 ± 9              | 6 ± 8              | 7 ± 7              | 8 ± 7              | 7 ± 7              | 8 ± 7              |
| Corr (r)          | 0.45               | 0.66               | 0.72               | 0.80               | 0.83               | 0.88               |
| 3-B               |                    |                    |                    |                    |                    |                    |
| Mean              | 12 ± 13            | 13 ± 17            | 11 ± 9$^c$         | 12 ± 8$^b$         | 11 ± 8$^b$         | 11 ± 9$^b$         |
| SEE               | 6 ± 4              | 6 ± 3              | 5 ± 3              | 5 ± 3              | 5 ± 3              | 5 ± 3              |
| Corr (r)          | 0.54               | 0.70               | 0.80               | 0.83               | 0.89               | 0.91               |
| 5-B               |                    |                    |                    |                    |                    |                    |
| Mean              | 12 ± 7$^c$         | 11 ± 6$^c$         | 11 ± 6$^b$         | 12 ± 6$^b$         | 11 ± 6$^b$         | 11 ± 6$^b$         |
| SEE               | 6 ± 4              | 5 ± 3              | 5 ± 4              | 4 ± 3              | 4 ± 4              | 4 ± 3              |
| Corr (r)          | 0.60               | 0.87               | 0.92               | 0.90               | 0.88               | 0.92               |
| 7-B               |                    |                    |                    |                    |                    |                    |
| Mean              | 13 ± 9             | 12 ± 9$^c$         | 11 ± 8$^b$         | 11 ± 7$^b$         | 12 ± 6$^b$         | 11 ± 7$^b$         |
| SEE               | 7 ± 5              | 7 ± 5              | 6 ± 5              | 7 ± 3              | 6 ± 5              | 6 ± 4              |
| Corr (r)          | 0.54               | 0.81               | 0.88               | 0.90               | 0.88               | 0.92               |

$^a$Exercise responses from each test were analyzed individually using KaleidaGraph, and the parameter estimates that were generated, and their SEE, were then averaged. $^b$(A) identifies the criterion measure (average of six $B$-values). (B) identifies means for which all individual differences (individual’s parameter estimate minus their criterion) fell within the limits of agreement that were calculated as $±1.0 \times$ SEE associated with the mean criterion measure $x \ (4 ± 3 \ s)$; in each case, these limits of agreement were approximately the same as limits that would be defined by the 95% confidence interval. The range of acceptable differences was $±4 \ s$ to $±4 \ s$, which represents the criterion value $±32 \%$. (C) identifies values for which all differences fell within the limits of agreement that were calculated as $±1.5 \times$ SEE; these limits of agreement were approximately the same as limits that would be defined by the 90% confidence interval. The acceptable range of differences was $±5 \ s$ to $±5 \ s$, which represents the criterion value $±48\%$.

Table 2. Estimates of $tau_{primary}$ (with Units of s) Generated Using the Results from the First Test, the First Two Tests, the First Three Tests, the First Four Tests, the First Five Tests, and All Six Tests$^a$, $^b$

| Type of Smoothing | Number of Values Averaged (Number of Tests Included in Calculation) |
|-------------------|---------------------------------------------------------------|
|                   | 1                  | 2                  | 3                  | 4                  | 5                  | 6                  |
| B × B             |                    |                    |                    |                    |                    |                    |
| Mean              | 45 ± 15            | 42 ± 13            | 43 ± 12            | 42 ± 12$^c$        | 43 ± 11$^c$        | 43 ± 11$^c$        |
| SEE               | 13 ± 9             | 13 ± 7             | 12 ± 7             | 11 ± 7             | 11 ± 7             | 11 ± 7             |
| Corr (r)          | 0.56               | 0.77               | 0.80               | 0.88               | 0.90               | 0.92               |
| 3-B               |                    |                    |                    |                    |                    |                    |
| Mean              | 44 ± 13            | 44 ± 11            | 43 ± 9$^c$         | 43 ± 8$^b$         | 43 ± 8$^b$         | 43 ± 8$^b$         |
| SEE               | 6 ± 4              | 6 ± 3              | 5 ± 3              | 5 ± 3              | 5 ± 3              | 5 ± 3              |
| Corr (r)          | 0.72               | 0.85               | 0.89               | 0.93               | 0.94               | 0.93               |
| 5-B               |                    |                    |                    |                    |                    |                    |
| Mean              | 43 ± 7$^c$         | 42 ± 6$^b$         | 42 ± 6$^b$         | 42 ± 6$^b$         | 42 ± 6$^b$         | 42 ± 6$^b$         |
| SEE               | 5 ± 4              | 5 ± 3              | 4 ± 4              | 4 ± 3              | 3 ± 4              | 3 ± 3              |
| Corr (r)          | 0.91               | 0.96               | 0.97               | 0.98               | 0.99               | Criterion          |
| 7-B               |                    |                    |                    |                    |                    |                    |
| Mean              | 42 ± 9             | 43 ± 9$^c$         | 42 ± 8$^b$         | 42 ± 7$^b$         | 42 ± 6$^b$         | 42 ± 7$^b$         |
| SEE               | 7 ± 5              | 6 ± 4              | 5 ± 4              | 5 ± 3              | 4 ± 4              | 5 ± 4              |
| Corr (r)          | 0.79               | 0.90               | 0.93               | 0.94               | 0.94               | 0.94               |

$^a$Exercise responses from each test were analyzed individually using KaleidaGraph, and the parameter estimates that were generated, and their SEE, were then averaged. $^b$(A) identifies the criterion measure (average of six $B$-values). (B) identifies means for which all individual differences (individual’s parameter estimate minus their criterion) fell within the limits of agreement that were calculated as $±1.0 \times$ SEE associated with the mean criterion measure $x \ (3 ± 3 \ s)$; in each case, these limits of agreement were approximately the same as limits that would be defined by the 85% confidence interval. The range of acceptable differences was $±3 \ s$ to $±3 \ s$, which represents the criterion value $±8\%$. (C) identifies values for which all differences fell within the limits of agreement that were calculated as $±1.5 \times$ SEE; these limits of agreement were approximately the same as limits that would be defined by the 90% confidence interval. The acceptable range of differences was $±5 \ s$ to $±5 \ s$, which represents the criterion value $±12\%$. 

Int J Sport Stud Hlth. 2019; 2(2):e98161.
Table 3. Estimates of $A_{primary}$ (with Units of mL/min) Generated Using the Results from the First Test, the First Two Tests, the First Three Tests, the First Four Tests, the First Five Tests, and All Six Tests$^{a, b}$

| Type of Smoothing | Number of Values Averaged (Number of Tests Included in Calculation) |
|-------------------|---------------------------------------------------------------|
|                   | 1 | 2 | 3 | 4 | 5 | 6 |
| **B × B**         |   |   |   |   |   |   |
| Mean              | 113 ± 503 | 1240 ± 460 | 1280 ± 435$^C$ | 1252 ± 442$^B$ | 1269 ± 435$^B$ | 1265 ± 433$^B$ |
| SEE               | 167 ± 80 | 150 ± 70 | 142 ± 57 | 145 ± 45 | 140 ± 40 | 143 ± 37 |
| Corr (r)          | 0.76 | 0.86 | 0.91 | 0.94 | 0.97 | 0.98 |
| **3 B**           |   |   |   |   |   |   |
| Mean              | 1293 ± 444 | 1108 ± 455$^C$ | 1294 ± 444$^C$ | 1281 ± 432$^B$ | 1265 ± 427$^B$ | 1273 ± 429$^B$ |
| SEE               | 93 ± 48 | 84 ± 39 | 82 ± 30 | 79 ± 3 | 78 ± 3 | 79 ± 3 |
| Corr (r)          | 0.82 | 0.93 | 0.95 | 0.95 | 0.98 | 0.98 |
| **5 B**           |   |   |   |   |   |   |
| Mean              | 1243 ± 467$^C$ | 1263 ± 446$^B$ | 1260 ± 438$^B$ | 1258 ± 430$^B$ | 1261 ± 426$^B$ | 1262 ± 425$^B$ |
| SEE               | 68 ± 21 | 64 ± 20 | 66 ± 18 | 67 ± 18 | 66 ± 17 | 68 ± 21 |
| Corr (r)          | 0.89 | 0.94 | 0.98 | 0.99 | 0.99 | 0.99 |
| **7 B**           |   |   |   |   |   |   |
| Mean              | 1269 ± 451 | 1229 ± 486$^C$ | 1244 ± 468$^B$ | 1251 ± 444$^A$ | 1255 ± 437$^B$ | 1257 ± 432$^B$ |
| SEE               | 75 ± 5 | 69 ± 5 | 68 ± 5 | 67 ± 3 | 67 ± 5 | 66 ± 4 |
| Corr (r)          | 0.88 | 0.86 | 0.94 | 0.96 | 0.99 | 0.99 |

$^a$ Exercise responses from each test were analyzed individually using KaleidaGraph, and the parameter estimates that were generated, and their SEE, were then averaged.

$^b$ (A) identifies the criterion measure (average of six 5-B values). (B) identifies means for which all individual differences (individual's parameter estimate minus their criterion) fell within the limits of agreement that were calculated as $±1.5\times$SEE associated with the mean criterion measure (68 ± 21 mL/min); in each case, these limits of agreement were approximately the same as limits that would be defined by the 85% confidence interval. The range of acceptable differences was 68 mL/min to +68 mL/min, which represents the criterion value ± 8%. Of note, 102 mL/min is approximately 1.4 mL/kg/min when expressed relative to body weight. Clearly, the two-component model identifies the $A_{primary}$ with very high precision.

Table 4. Estimates of $T_{D_{hemia}}$ (with Units of s) Generated Using the Results from the First Test, the First Two Tests, the First Three Tests, the First Four Tests, the First Five Tests, and All Six Tests$^{a, b}$

| Type of Smoothing | Number of Values Averaged (Number of Tests Included in Calculation) |
|-------------------|---------------------------------------------------------------|
|                   | 1 | 2 | 3 | 4 | 5 | 6 |
| **B × B**         |   |   |   |   |   |   |
| Mean              | 119 ± 15 | 127 ± 13 | 125 ± 12$^C$ | 127 ± 12$^C$ | 126 ± 11$^B$ | 126 ± 10$^B$ |
| SEE               | 22 ± 9 | 21 ± 7 | 19 ± 7 | 19 ± 7 | 18 ± 7 | 19 ± 7 |
| Corr (r)          | 0.56 | 0.77 | 0.85 | 0.88 | 0.90 | 0.92 |
| **3 B**           |   |   |   |   |   |   |
| Mean              | 118 ± 13 | 118 ± 13$^B$ | 121 ± 9$^B$ | 123 ± 8$^C$ | 124 ± 8$^B$ | 124 ± 8$^B$ |
| SEE               | 11 ± 4 | 11 ± 3 | 10 ± 3 | 10 ± 3 | 10 ± 3 | 10 ± 3 |
| Corr (r)          | 0.72 | 0.86 | 0.89 | 0.93 | 0.94 | 0.93 |
| **5 B**           |   |   |   |   |   |   |
| Mean              | 121 ± 17$^C$ | 117 ± 16$^B$ | 118 ± 16$^B$ | 120 ± 14$^B$ | 120 ± 15$^B$ | 120 ± 14$^B$ |
| SEE               | 10 ± 4 | 6 ± 3 | 7 ± 4 | 6 ± 3 | 6 ± 4 | 6 ± 3 |
| Corr (r)          | 0.91 | 0.96 | 0.97 | 0.98 | 0.99 | 0.99 |
| **7 B**           |   |   |   |   |   |   |
| Mean              | 127 ± 22 | 121 ± 19$^B$ | 118 ± 18$^C$ | 118 ± 17$^B$ | 119 ± 14$^B$ | 118 ± 16$^B$ |
| SEE               | 8 ± 5 | 9 ± 4 | 8 ± 4 | 8 ± 3 | 7 ± 4 | 8 ± 4 |
| Corr (r)          | 0.79 | 0.88 | 0.93 | 0.96 | 0.96 | 0.95 |

$^a$ Exercise responses from each test were analyzed individually using KaleidaGraph, and the parameter estimates that were generated, and their SEE, were then averaged.

$^b$ (A) identifies the criterion measure (average of six 5-B values). (B) identifies means for which all individual differences (individual's parameter estimate minus their criterion) fell within the limits of agreement that were calculated as $±1.5\times$SEE associated with the mean criterion measure (6 ± 3 s); in each case, these limits of agreement were approximately the same as limits that would be defined by the 85% confidence interval. The range of acceptable differences was 6 s to +6 s, which represents the criterion value ± 5%. (C) identifies values for which all differences fell within the limits of agreement that were calculated as $±1.5\times$SEE; these limits of agreement were approximately the same as limits that would be defined by the 90% confidence interval. The acceptable range of differences was -102 mL/min to +102 mL/min, which represents the criterion value ± 8%. Of note, 102 mL/min is approximately 1.4 mL/kg/min when expressed relative to body weight. Clearly, the two-component model identifies the $T_{D_{hemia}}$ with very high precision.
are summarized in the tables and can be explained as follows: mean values from type-of-smoothing × number-of-tests combinations for which all individual values fell within very strict limits of agreement (±1.0 × SEE) are identified by superscript ‘B’ and mean values for which all individual values fell within 50% broader limits of agreement are identified by superscript ‘C’. So, for example, for the 5-B $\tau_{\text{primary}}$ parameter value obtained using only data from the first test, all individual values fell within 5 s (1.5 × SEE) of their associated criterion value; when parameter values from the first two tests were averaged, all fell within 3 s (1.0 × SEE). This can be interpreted that a single test provides enough 5-B data to closely identify (within 5 s) the value of the $\tau_{\text{primary}}$ parameter and that, with data from two tests, individual values will be within 3 s of the ‘true’ value. Requiring more tests produces rapidly diminishing returns; we cannot even argue that accuracy and precision of these values improves when data from more than two or three tests were included in their calculation.

### 5. Discussion

The important finding in the present study is that curve fitting of 5-B data from only one exercise test can generate accurate values for parameters of the two-component $\text{VO}_2$ response profile in heavy intensity exercise. 3-B and 7-B smoothing methods were also very good to improve the signal-to-noise ratio and reduce the number of tests that must be performed. The use of two or three tests may be indicated if acceptable tolerance of deviation from the ‘true’ value of each parameter is very small, for example, less than 3 s for $\tau_{\text{primary}}$, < 1 mL/kg/min for $A_{\text{primary}}$, < 6 s for $\text{T}_D_{\text{primary}}$, and < 1 mL/kg/min for $A_{\text{primary}}$. Slightly better accuracy may be obtained if more tests are performed, but any improvements may not justify the extra demands on personnel, participants, and other resources.

Subsequent to the work of Larmorra and colleagues (10), it has often been assumed that multiple trials are required to minimize the signal-to-noise ratio, and often this is accomplished by combining data from the trials before smoothing the data, that is, before fitting them to a mathematical model (8). Benson and colleagues (8) applied a variety of smoothing interventions to one to ten sets of simulated moderate intensity. Like Francescato and colleagues (17), who also used simulated data, they found little difference between the effects of smoothing. They did report that four trials were optimal. They also found that combining data before modeling was superior to modeling and then combining the results (i.e., averaging the parameter estimates from different tests, as we did in the present study.) However, they noted that modeling results from tests individually and then averaging the results has been proposed and used (18) and may be statistically more appropriate (19). We note, that this method also allows the investigator to evaluate whether there is a trend in the results. i.e., to determine if responses are changing over time (they were not, in the present study).

In a study similar to the present study, Keir and col-

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**Table 5. Estimates of $A_{\text{primary}}$ (with Units of mL/min) Generated Using the Results from the First Test, the First Two Tests, the First Three Tests, the First Four Tests, the First Five Tests, and All Six Tests**

| Type of Smoothing | Number of Values Averaged (Number of Tests Included in Calculation) |
|-------------------|---------------------------------------------------------------|
| B × B             |                                                              |
| Mean              | 448 ± 113 b                                                   |
| Corr (r)          | 0.70, 0.83, 0.91, 0.95, 0.97, 0.96                             |
| 3-B               |                                                              |
| Mean              | 454 ± 99                                                     |
| Corr (r)          | 0.82, 0.93, 0.95, 0.95, 0.96, 0.98                             |
| 5-B               |                                                              |
| Mean              | 460 ± 89 c                                                   |
| Corr (r)          | 0.86, 0.94, 0.98, 0.99, 0.99, Criterion                      |
| 7-B               |                                                              |
| Mean              | 466 ± 97 c                                                   |

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$^a$Exercise responses from each test were analyzed individually using KaleidaGraph, and the parameter estimates that were generated, and their SEE, were then averaged. $^b$A identifies the criterion measure (average of six 5-B values). There were no SEE associated with the MRT parameter, because it was calculated from the values of $\tau_{\text{primary}}$ and $A_{\text{primary}}$; we chose to use the same values for this amplitude as were calculated for the $A_{\text{primary}}$ parameter. (B) identifies means for which all individual differences (individual’s parameter estimate minus their criterion) fell within the limits of agreement that were calculated as ±1.0 mL/min, which represents the criterion value ±~15%. (C) identifies values for which all differences fell within the limits of agreement that were calculated as ±1.5 mL/min, which represents the criterion value ±~22%. Of note, 68 mL/kg and 102 mL/min are less than 1.0 mL/kg/min and 1.5 mL/kg/min, respectively.
leagues (9) evaluated the effects of several smoothing techniques applied to data from four identical moderate intensity exercise tests (i.e., assuming that combining data from four tests was requisite for obtaining data with good precision). They concluded that modeling had no effect on the mean values for the parameter estimates but that it did affect the precision of the estimates, as judged by the 95% confidence intervals. Differences between their study and ours include that we used stricter confidence intervals, we tested the effect of performing multiple trials (rather than limiting analyses to data combined from all the trials that were performed), and we used data from heavy intensity exercise, rather than sub-threshold moderate intensity exercise. We fitted data to a two-component model, so that the effect of smoothing and the effect of number of trials was determined for primary phase and slow component parameters. Given the greater complexity of the response and greater number of parameters, compared to studies which used only a mono-exponential response, less precision might be expected around the parameter estimates generated in the present study. The good precision and accuracy that we report may reflect that our participants were familiar with exercise testing while breathing through a mouthpiece.

5.1. Conclusions

The accuracy and precision of estimates of the parameters of the primary and slow phases of the VO\(_2\) response during heavy intensity exercise can be improved by using data from more than one test and by smoothing the data prior to fitting them to an appropriate mathematical model. Depending upon the accuracy required, that is depending upon how close each and every participant’s value must be to his or her ‘true’ value, smoothed data from one or two tests is sufficient to calculate the values that describe the two-parameter VO\(_2\) response profile in heavy intensity cycling exercise.

Acknowledgments

The contribution of Dr. Daniela Pedini to collection of data from the first fourteen research participants and the efforts of all participants made this study possible.

Footnotes

Authors’ Contribution: The author was responsible for designing the study, collecting and analyzing the data, and preparing the manuscript.

Conflict of Interests: No conflict of interests.

Ethical Approval: The study was approved by the Institutional Review Board for the Protection of Human Subjects in Research at the University of North Texas.

Funding/Support: No funding.

Informed Consent: Participants participate and provided informed consent.

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