Measurement of $D_s^+$ and $D_s^{*+}$ production in $B$ meson decays and from continuum $e^+e^-$ annihilations at $\sqrt{s} = 10.6$ GeV

The BABAR Collaboration

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Abstract

New precise measurements of $D_s^+$ and $D_s^{*+}$ meson production from $B$ mesons and $q\bar{q}$ continuum events near the $\Upsilon(4S)$ resonance are presented in this paper. Using the BABAR data recorded in 1999 and 2000 of 20.8 fb$^{-1}$ on-resonance and 2.6 fb$^{-1}$ off-resonance, we measure the inclusive branching fractions $\mathcal{B}(B \rightarrow D_s^+ X) = (10.93 \pm 0.19 \pm 0.58 \pm 2.73)\%$ and $\mathcal{B}(B \rightarrow D_s^{*+} X) = (7.94 \pm 0.82 \pm 0.72 \pm 1.99)\%$, where the first error is statistical, the second is the systematic error, and the third is the error due to the $D_s^+ \rightarrow \phi \pi^+$ branching fraction uncertainty. The branching fractions $\Sigma\mathcal{B}(B \rightarrow D_s^{(*)+} \bar{D}^{(*)}) = (5.07 \pm 0.09 \pm 0.34 \pm 1.27)\%$ and $\Sigma\mathcal{B}(B \rightarrow D_s^{*+} \bar{D}^{(*)}) = (4.07 \pm 0.42 \pm 0.53 \pm 1.02)\%$ have been determined from the measured $D_s^{(*)+}$ momentum spectra.

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1 Introduction

The study of $D_s^{(*)+}$ meson production in $B$ decays allows exploration of the mechanisms leading to the creation of $c\bar{s}$ quark pairs. Although several Feynman diagrams could lead to $D_s^{(*)+}$ mesons in $B$ decays, the spectator diagram (Fig. 1) is expected to dominate. In addition, $D_s^{(*)+}$ mesons could be produced from $c\bar{c}$ continuum events. It has been pointed out [1] that the rate from $B$ decays may be large. This might help to explain some of the theoretical difficulties [2] in accounting simultaneously for the total inclusive $B$ decay rate and the semileptonic branching fraction of the $B$ meson. The measurement of the $D_s^{(*)+}$ momentum allows a determination of the fraction of two-body and multi-body decay modes, which will aid understanding $b \to c\bar{s}q$ transitions.

In this paper, measurements of $B \to D_s^{(*)+}X$ and $B \to D_s^{(*)+}X$ production rates and momentum spectra are presented. These mesons are reconstructed using the decays $D_s^+ \to \phi \pi^+$ and $D_s^{*+} \to D_s^+\gamma$.

![Spectator Diagram](image)

Figure 1: The main spectator diagram leading to the production of $D_s^{(*)+}$ mesons in $B$ decays.

2 The BABAR detector and data set

The data used for this analysis were collected with the BABAR detector [3] at the PEP-II asymmetric-energy collider [4] at the Stanford Linear Accelerator center. An integrated luminosity of 20.8 fb$^{-1}$ was recorded corresponding to about 22.7 million produced $B\bar{B}$ pairs at the $\Upsilon(4S)$ resonance (“on-resonance”) and 2.6 fb$^{-1}$ at an energy about 40 MeV below the $B\bar{B}$ threshold (“off-resonance”). Since a detailed description of the BABAR detector is presented in Ref. [3], only the components of the detector most crucial to this analysis are briefly summarized below.

Charged particles are detected and their momenta measured by a combination of a central drift chamber (DCH) with a helium-based gas and a five-layer (double-sided) silicon vertex tracker (SVT), within a 1.5 T solenoidal field produced by a superconducting magnet. The tracking system covers a solid angle of 92% in the center-of-mass frame. Charged particles are identified using the ionization energy loss ($dE/dx$) measured in the DCH and SVT and the Cherenkov radiation detected in a ring imaging Cherenkov device (DIRC). Photons are identified by the CsI electromagnetic calorimeter.

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1Reference in this paper to a specific decay channel or state also implies the charge conjugated decay or state. The notation $D_s^{(*)+}$ means either $D_s^{(*)}$ or $D_s^{(*)+}$. $B \to D_s^{(*)+}\overline{D}^{(*)}$ is a general representation of any of modes with $c\bar{s}$, $\bar{c}q$ including their excited states.
3 $D_s^+$ and $D_s^{*+}$ selection

The analysis reported here uses only the decay mode $D_s^+ \rightarrow \phi \pi^+$, with $\phi \rightarrow K^+K^-$, as this channel offers the best signal-to-background ratio. The charged tracks are required to originate from within ±10 cm along the beam direction and ±1.5 cm in the transverse plane of the interaction point and leave at least 12 hits in the drift chamber.

In order to obtain a sufficiently clean sample, kaon identification is required for the tracks forming the $\phi$ meson by using $dE/dx$ information from DCH and SVT and the Cherenkov angle and the number of photons as measured by the DIRC. The kaon selection is based on the likelihoods given by each detector and uses, for each track, the ratio of likelihoods for the pion and the kaon mass hypotheses, $L_\pi/L_K$. If this ratio is less than unity for at least one of the considered subsystems, the particle is selected as a kaon. The DIRC is used both in a positive identification mode and also in a veto mode for the case where a kaon with the measured track momentum would not be above the Cherenkov threshold. A tighter level of identification is also available using a total likelihood defined as the product of the likelihoods of each subsystem. In this case the track is tagged as a kaon if the ratio of the total likelihoods for the pion and kaon mass hypotheses is less than unity.

Three charged tracks originating from a common vertex are combined to form a $D_s^+$ candidate. Two oppositely charged tracks have to be identified as kaons by satisfying the basic criteria and at least one of them has to satisfy the tighter selection. The $K^+K^-$ invariant mass must be within 8 MeV/$c^2$ of the nominal $\phi$ mass [5]. In this particular decay, the $\phi$ meson is polarized longitudinally and therefore the angular distribution of the kaons has a $\cos^2 \theta_H$ dependence, where $\theta_H$ is the angle between the $K^+$ and $D_s^+$ in the $\phi$ rest frame. This angle is required to satisfy $|\cos \theta_H| > 0.3$, thereby keeping 97.5% of the signal while rejecting about 30% of the background.

Using the selection described above, a clean $D_s^+$ signal of 47794±311 events is observed (Fig. 4). A clear signal for the Cabibbo-suppressed decay mode $D^+ \rightarrow \phi \pi^+$ is also observed.

$D_s^{*+}$ mesons are reconstructed using the decay $D_s^{*+} \rightarrow D_s^+\gamma$, with the subsequent decay $D_s^+ \rightarrow \phi \pi^+$. $D_s^+$ candidates are selected by requiring the $\phi\pi$ invariant mass to be within 2.5 standard deviations ($\sigma$) of the peak value. These are then combined with the “single photons” of the event, which are required to satisfy $E_\gamma > 50$ MeV, where $E_\gamma$ is the photon energy in the laboratory frame, and $E_\gamma^* > 110$ MeV, where $E_\gamma^*$ is the photon energy in the $\Upsilon(4S)$ rest frame. In order to reduce the combinatoric background, the candidate photon should not form a $\pi^0$, defined by a total energy $E_{\gamma\gamma}^* > 200$ MeV and an invariant mass $115 < M_{\gamma\gamma} < 155$ MeV/$c^2$, when combined with any other photon in the event. The distribution of the mass difference $\Delta M = M_{D_s^{*+}} - M_{D_s^+}$ is shown in Fig. 3. A clear peak with 14392 ± 376 events is observed.

4 Extraction of the $D_s^{(*)+}$ momentum spectra

The momentum spectrum of $D_s^+$ mesons in the $\Upsilon(4S)$ rest frame is extracted by fitting the $\phi\pi$ invariant mass distribution in each momentum bin. The bins are chosen to be 200 MeV/$c$ wide, which is much larger than the momentum resolution ($\approx 6$ MeV/$c$). The fit function is a single Gaussian for each of the $D_s^+$ and the $D^+$ signals, with the constraint of a common width. The combinatorial background is accounted for by an exponential. As there are many more events for the on-resonance data, the number of $D_s^+$ in the off-resonance data is extracted with the same fit function but with $M_{D^+}$, $M_{D_s^+}$ and $\sigma$ fixed to the values obtained from the binned chi-squared fit to the on-resonance data.
Figure 2: The observed $\phi\pi$ invariant mass spectrum. The lower mass peak corresponds to the Cabibbo-suppressed decay mode $D^+ \rightarrow \phi\pi^+$. The fit function is a single Gaussian for each peak, with their widths constrained to be equal, on top of an exponential background.

Figure 3: Distribution of the $\Delta M = M_{D^+_s\gamma} - M_{D^+_s}$ mass difference. The fit function is a Crystal Ball function for the signal on top of a threshold function, as described in text.

In the same way as for $D_s^+$, the momentum spectrum of $D_s^{*+}$ mesons in the $\Upsilon(4S)$ rest frame is extracted by fitting the $\Delta M$ invariant mass distribution for 250 MeV/c wide momentum bins. The $\Delta M$ distribution for the signal is characterized by an asymmetric shape to account for energy leakage and shower shape fluctuations. The fit function for the signal is the Crystal Ball function [6]. For the background, a threshold function

$$f(\Delta M) = p_1 (\Delta M - p_2)^{p_3} e^{p_4(\Delta M - p_2)}$$

is used, with the four free parameters $p_i$ being determined from the fit. After ensuring that the connection point between the Gaussian and power-law tail of the Crystal Ball function does not depend on momentum and agrees with the Monte Carlo, this parameter has been fixed at $0.89\sigma$ in the final fit. The off-resonance data are again fit with the signal shape parameters $\Delta M$ and $\sigma$ fixed to the values obtained from the fit to the on-resonance data.

The uncertainty on the shape of the background leads to an additional systematic error. This error is estimated by using different parameterizations for the background shape.

The efficiency obtained from Monte Carlo with generic $B\overline{B}$ and $c\bar{c}$ events varies as a function of the $D_{s^{(*)}+}$ momentum ($p^*$) in the $\Upsilon(4S)$ rest frame and ranges from 20% when the $D_{s^+}$ is at rest to 40% for $p^* = 5$ GeV/c, and from 5% to 20% for $D_{s^{*+}}$. The number of reconstructed $D_{s^+}$ and $D_{s^{*+}}$ is corrected bin-by-bin for the efficiency. The efficiency-corrected number of $D_{s^+}$ and $D_{s^{*+}}$ as a function of their momentum in the $\Upsilon(4S)$ rest frame is shown in Fig. [4].
The $D_{s}^{+}$ and $D_{s}^{*+}$ cross sections for production from the $q\bar{q}$ continuum are obtained by integrating the spectrum obtained from the off-resonance data. This gives the preliminary results

$$\sigma(e^+e^- \to D_{s}^{\pm}X) \times B(D_{s}^{\pm} \to \phi\pi^+) = 7.55 \pm 0.20 \pm 0.34 \text{ pb}$$

and

$$\sigma(e^+e^- \to D_{s}^{*\pm}X) \times B(D_{s}^{*\pm} \to \phi\pi^+) = 5.79 \pm 0.66 \pm 0.50 \text{ pb}.$$

The off-resonance data are scaled according to the luminosity ratio and then subtracted bin-by-bin from the on-resonance data in order to find the $D_{s}^{(*)+}$ momentum spectra from $B$ meson decays. It is important to note that, with this method, the result is independent of any assumption about the shape of the fragmentation function, and most of the systematic errors due to the background parameterization cancel. Integrating the spectrum after continuum subtraction gives a total $D_{s}^{+}$ yield from $B$ meson decays of 87711±1485. This corresponds to the inclusive preliminary branching fraction

$$B(B \to D_{s}^{+}X) = \left[ (10.93 \pm 0.19 \pm 0.58) \times \frac{3.6 \pm 0.9\%}{B(D_{s}^{+} \to \phi\pi^+)} \right] \%.$$ 

The total $D_{s}^{*+}$ yield from $B$ meson decays is 60047±6201 events, leading to the inclusive preliminary branching fraction

$$B(B \to D_{s}^{*+}X) = \left[ (7.94 \pm 0.82 \pm 0.72) \times \frac{3.6 \pm 0.9\%}{B(D_{s}^{+} \to \phi\pi^+)} \right] \%.$$ 

In the results above, the first error is statistical, the second is the systematic error and the third error, which is dominant, is due to the uncertainty in the $D_{s}^{+} \to \phi\pi^+$ branching fraction [3]. The

5 Branching fractions

Figure 4: The (a) $D_{s}^{+}$ and (b) $D_{s}^{*+}$ efficiency-corrected momentum spectra for on-resonance data (solid circles) and for scaled off-resonance data (open circles).
Table 1: Systematic errors for $B \rightarrow D_s^{(*)+} X$

| Source                        | Fractional Error on $B$ (%) |
|-------------------------------|-----------------------------|
|                               | $B \rightarrow D_s^+ X$    |
|                               | $B \rightarrow D_s^{(*)+} X$ |
| Signal shape                  | 0.5                         |
| Background parameterization   | 0.4                         |
| Monte Carlo statistics        | 2.5                         |
| Bin width                     | 1.4                         |
| Total for $D_s^+$ yield       | 2.9                         |
| Number of $BB$ events         | 1.6                         |
| $\mathcal{B}(\phi \rightarrow K^+K^-)$ | 1.6                 |
| Particle id efficiency        | 1.0                         |
| Tracking efficiency           | 3.6                         |
| $\mathcal{B}(D_s^{(*)+} \rightarrow D_s^+ \gamma)$ | 2.7               |
| Photon efficiency             | 1.3                         |
| $\pi^0$ veto                  | 2.7                         |
| Total systematic error        | 5.3                         |
|                               | 9.0                         |

Various contributions to the systematic error are listed in Table 1. One of the dominant systematic errors is the 3.6% total uncertainty due to our knowledge of the tracking efficiency (1.2% per track for the decay chain $D_s^+ \rightarrow \phi \pi^+, \phi \rightarrow K^+K^-$).

6 Fits to $D_s^{(*)+}$ momentum spectra

In the $\Upsilon(4S)$ rest frame, two-body $B$ decays produce $D_s^{(*)+}$ mesons with a flat momentum spectrum over a 300 MeV/c wide range. In $B$ decays, the $D_s^{(*)+}$ momentum spectrum is essentially governed by the production of direct $D_s^{(*)+}$. Other $c\bar{s}$ states such as $D_{s1}(2536)$ and $D_{s2}(2573)$ primarily decay to $D^{(*)} K$. Because $D_s^{(*)+}$ decays to $D_s^+ \gamma$ or $D_s^+ \pi^0$, the $D_s^+$ momentum distribution is slightly broader and shifted downward compared to direct production from $B \rightarrow D_s^+ X$.

In fitting the observed momentum spectra, three different sources of $D_s^{(*)+}$ mesons in $B$ decays are considered:

1. $B \rightarrow D_s^{(*)+} \bar{D}^{(*)}$ decays. The relative branching fractions of the individual channels can be taken either from existing measurements or from predictions assuming factorization. The fit is performed for both cases, with the assumption $f_{D_s^{(*)+}} = f_{D_s^+}$ for the theoretical models, where $f_{D_s^{(*)+}}$ are the $D_s^{(*)+}$ decay constants.

2. $B \rightarrow D_s^{(*)+} \bar{D}_s^{(*)}$ decays. The contributions from $B \rightarrow D_s^{(*)+} \bar{D}_s^0 (j = 1/2)$, $B \rightarrow D_s^{(*)+} \bar{D}_1(2420)$, $B \rightarrow D_s^{(*)+} \bar{D}_1(j = 1/2)$ and $B \rightarrow D_s^{(*)+} \bar{D}_2(2460)$ are included in this source.

3. Three-body $B \rightarrow D_s^{(*)+} \bar{D}^{(*)} \pi/\rho/\omega$ decays. Since little is known on these decays, they are attributed an equal weight and the momentum distributions are generated according to phase space.
Figure 5: The fit result for (a) $D_s^+$ and (b) $D_s^{(*)+}$ momentum spectra. The data are dots with error bars, the histograms are the components of the fit function described in the text. Type (1) is $B \rightarrow D_s^{(*)+} \overline{D}(s)$, Type (2) is $B \rightarrow D_s^{(*)+} \overline{D}^{**}$ and Type (3) is $B \rightarrow D_s^{(*)+} \overline{D}(s) \pi/\rho/\omega$. The solid histogram is the sum of three components.

As a result of a chi-squared fit of $D_s^+$ momentum spectrum with these components, the ratio of two-body modes to the total inclusive rate is determined to be

$$\frac{\Sigma B(B \to D_s^{(*)+} \overline{D}(s))}{B(B \to D_s^+ X)} = (46.4 \pm 1.9 \pm 0.6)\%,$$

where the first error is statistical and the second is due to model uncertainty. This last is obtained from the variation of the fit result with different individual contributions from the modes included with each of the three sources of $D_s^+$ mesons, as discussed below. From the fit to the $D_s^{(*)+}$ momentum spectrum, we find

$$\frac{\Sigma B(B \to D_s^{(*)+} \overline{D}(s))}{B(B \to D_s^{(*)+} \overline{D}(s))} = (53.3 \pm 4.5 \pm 1.6 \pm 2.1)\%,$$

where the first error is statistical, the second error represents the systematic uncertainty due to the background parameterization (negligible for $B \to D_s^{(*)+} \overline{D}(s)$), and the third error is due to model uncertainty obtained as for $B \to D_s^{(*)+} \overline{D}(s)$.

The fit is performed under different assumptions for the relative contributions of the modes in source (1), varied according to the theoretical predictions and measurements. Different weights of $B \to D_s^{(*)+} \overline{D}^{**}$ and $B \to D_s^{(*)+} \overline{D}^{**}$, as well as different relative branching fractions of the four modes within source (2), are also used. In source (3), two cases are considered: either $B \to D_s^{(*)+} \overline{D}(s) \pi$ or $B \to D_s^{(*)+} \overline{D}(s) \rho/\omega$ is assumed to be dominant. The best $\chi^2$ for the fit to the inclusive $D_s^{(*)+}$ momentum spectrum is obtained when the contribution from $B \to D_s^{(*)+} \overline{D}(s) \rho/\omega$ is dominant.
compared to \( B \rightarrow D_s^{(*)} \bar{D}^{(*)} \pi \). The results of the fits to the \( D_s^{(*)}+ \) momentum spectra are shown in Fig. 3 for one of the assumptions.

Using the fit results and the relative rates for \( B \rightarrow D_s^{(*)} \bar{D}^{(*)} \) we find the preliminary results

\[
\Sigma B(B \rightarrow D_s^{(*)}+ \bar{D}^{(*)}) = (5.07 \pm 0.09 \pm 0.34 \pm 1.27)\%,
\]

\[
\Sigma B(B \rightarrow D_s^{*+} \bar{D}^{(*)}) = (4.07 \pm 0.42 \pm 0.53 \pm 1.02)\%.
\]

where the errors from the fits to the momentum spectra are added in quadrature with the systematic error due to the \( D_s^{(*)} \rightarrow \phi \pi^+ \) branching fraction uncertainty.

7 Summary

In summary, preliminary branching fractions for inclusive \( B \rightarrow D_s^{(*)}+X \) production have been determined to be \( B(B \rightarrow D_s^+X) = (10.93 \pm 0.19 \pm 0.58 \pm 2.73)\% \) and \( B(B \rightarrow D_s^{*+}X) = (7.94 \pm 0.82 \pm 0.72 \pm 1.99)\% \). The \( D_s^{(*)}+ \) cross sections from \( \phi \) continuum events at about 40 MeV below \( \Upsilon(4S) \) mass are \( \sigma(e^+e^- \rightarrow D_s^+X) \times B(D_s^+ \rightarrow \phi \pi^+) = 7.55 \pm 0.20 \pm 0.34 \) pb and \( \sigma(e^+e^- \rightarrow D_s^{*+}X) \times B(D_s^{*+} \rightarrow \phi \pi^+) = 5.79 \pm 0.66 \pm 0.50 \) pb. Our results for \( D_s^+ \) are in agreement with previous measurements \[1, 4\], although with considerable improvement in accuracy. In contrast to previous measurements, our results do not rely on any assumptions concerning the shape of the fragmentation function.

From a fit to the \( D_s^{(*)}+ \) momentum spectra, preliminary results have been obtained for the fraction of all two-body \( B \rightarrow D_s^{(*)}+ \bar{D}^{(*)} \) decays relative to the total inclusive \( D_s^+ \) yield \((46.4 \pm 1.9 \pm 0.6)\% \) and for all \( B \rightarrow D_s^{*+} \bar{D}^{(*)} \) decays relative to the total inclusive \( D_s^{*+} \) yield \((53.3 \pm 4.5 \pm 1.6 \pm 2.1)\% \), where the last error includes the model dependence. Combining these results gives \( \Sigma B(B \rightarrow D_s^{(*)}+ \bar{D}^{(*)}) = (5.07 \pm 0.09 \pm 0.34 \pm 1.27)\% \) and \( \Sigma B(B \rightarrow D_s^{*+} \bar{D}^{(*)}) = (4.07 \pm 0.42 \pm 0.53 \pm 1.02)\% \)

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The $\Delta M$ distribution for the $D^+_s\gamma$ signal is fit with the Crystal Ball function

$$f(x) = N \cdot \left\{ \begin{array}{ll}
\exp\left(-\frac{(x-\bar{x})^2}{2\sigma^2}\right) & ; (x-\bar{x})/\sigma > \alpha \\
A \times (B - \frac{x-\bar{x}}{\sigma})^{-n} & ; (x-\bar{x})/\sigma \leq \alpha
\end{array} \right.$$ 

where $A \equiv \left(\frac{n}{|\alpha|}\right)^n \times \exp(-|\alpha|^2/2)$ and $B \equiv \frac{n}{|\alpha|} - |\alpha|$. $N$ is a normalization factor, $\bar{x}$ and $\sigma$ are the peak position and width of the Gaussian portion of the function, $\alpha$ is the point at which the function changes to the power function and $n$ is the exponent of the power function. $A$ and $B$ are defined such as to maintain the continuity of the function and it first derivative at $\alpha$. More details can be found in D. Antreasyan, Crystal Ball Note 321 (1983).