Orbital transmutation and the electronic spectrum of FeSe in the nematic phase

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(Dated: March 24, 2022)

We consider the electronic spectrum near $M = (\pi, \pi)$ in the nematic phase of FeSe ($T < T_{\text{nem}}$) and make a detailed comparison with recent ARPES and STM experiments. Our main focus is the unexpected temperature dependence of the excitations at the $M$ point. These have been identified as having $xz$ and $yz$ orbital character well below $T_{\text{nem}}$, but remain split at $T > T_{\text{nem}}$, in apparent contradiction to the fact that in the tetragonal phase the $xz$ and $yz$ orbitals are degenerate. Here we present two scenarios which can describe the data. In both scenarios, hybridization terms present in the tetragonal phase leads to an orbital transmutation, a change in the dominant orbital character of some of the bands, between $T > T_{\text{nem}}$ and $T < T_{\text{nem}}$. The first scenario relies on the spin-orbit coupling at the $M$ point. We show that a finite spin-orbit coupling gives rise to orbital transmutation, in which one of the modes, identified as $xz$ ($yz$) at $T < T_{\text{nem}}$, becomes predominantly $xy$ at $T > T_{\text{nem}}$ and hence does not merge with the predominantly $yz$ ($xz$) mode. The second scenario, complementary to the first, takes into consideration the fact that both ARPES and STM are surface probes. In the bulk, a direct hybridization between the $xz$ and $yz$ orbitals is not allowed at the $M$ point, however, it is permitted on the surface. In the presence of a direct $xz/yz$ hybridization, the orbital character of the $xz/yz$ modes changes from pure $xz$ and pure $yz$ at $T < T_{\text{nem}}$ to $xz \pm yz$ at $T > T_{\text{nem}}$, i.e., the two modes again have mono-orbital character at low $T$, but do not merge at $T_{\text{nem}}$. We discuss how these scenarios can be distinguished in polarized ARPES experiments.

I. INTRODUCTION

The intriguing physical properties of FeSe continue to attract the attention of the correlated electron systems community [1,3]. This material has the simplest structure among the Fe-based superconductors (FeSCs), yet its phase diagram is rather complex, particularly under pressure [4,5], and is quite different from that of other FeSCs. The most notable distinction is a wide temperature range where the tetragonal symmetry of the lattice is spontaneously broken down to $C_2$ (the nematic phase). The nematic order emerges at $T_{\text{nem}} \sim 90$ K at nominal pressure, and is not accompanied by a stripe magnetic order [6]. Superconductivity emerges at a much smaller temperature, and is not accompanied by a stripe magnetic order [6]. Superconductivity emerges at much smaller temperature, and is not accompanied by a stripe magnetic order [6]. Superconductivity emerges at much smaller $T \sim 8$ K [7].

The electronic structure of FeSe in the tetragonal phase ($T > T_{\text{nem}}$) is fairly typical of the FeSCs – there are two cylindrical hole pockets centered at $\Gamma = (0, 0, 0)$ in the Brillouin zone (BZ) and two cylindrical electron pockets [3]. In the 1-Fe BZ, one of the electron pockets is centered at $(\pi, 0)$ (the X point), while the other is centered at $(0, \pi)$ (the Y point) [8]. The hole pockets consist equally of fermions from the $xz$ and $yz$ orbitals, the X pocket is made of fermions from the $y$ and $xz$ orbitals, and the Y pocket of fermions from the $xz$ and $xy$ orbitals [3]. In the crystallographic 2-Fe unit cell, the X and Y pockets are folded onto $M = (\pi, \pi)$, or, equivalently, $M' = (\pi, -\pi)$, and form inner and outer pockets [9]. The inner pocket is made mostly of $xz$ and $yz$ fermions, and the outer pocket is made mostly of $xy$ fermions [3]. The two pockets touch along high-symmetry axes in the absence of spin-orbit coupling (SOC) and split in its presence [10-12]. Although the same geometry of low-energy excitations holds in other FeSCs, the peculiarity of FeSe is that the Fermi energies for the hole and electron bands are smaller than in other FeSCs [13,18].

In the nematic phase, the occupations of the $xz$ and $yz$ orbitals become inequivalent on both hole and electron pockets [19], and the occupations of the $xy$ orbitals at $X$ and at $Y$ also generally become different (the latter gives rise to a hopping anisotropy in real space [20]). This changes both the shape of the pockets and the orbital composition of excitations along them. Of the two hole pockets, the smaller one sinks below the Fermi level, and the larger one becomes elliptical [19,21,22]. The direction of its longer axis (towards $X$ or $Y$ in the 1-Fe BZ, or, equivalently, towards $M$ or $M'$ in the 2-Fe BZ) is chosen spontaneously. In non-strained (twinned) samples, Angle Resolved Photo-Emission Spectroscopy (ARPES) measurements necessarily see a superposition of the two hole pockets elongated along orthogonal directions, due to the presence of twin domains [18]. However, polarized ARPES measurements on twinned samples or unpolarized measurements in detwinned samples allow one to focus on a single domain. Here, we follow ARPES data and focus on the domain in which, deep in the nematic phase, the hole pocket is elongated towards $Y$ in the 1-Fe BZ [21,24], or, equivalently, along $\Gamma - M'$ in the 2-Fe BZ (we use the convention that $\Gamma - Y$ direction in the 1-Fe BZ corresponds to $\Gamma - M'$ in the 2-Fe BZ, see Fig. 1 for an explanation of the relationship between the 1- and 2-Fe unit cells [9].) For the electron pockets, both ARPES [21,25,27] and Scanning Tunneling Microscopy (STM) measurements [2] have shown that, within the same domain, the inner electron pocket acquires a peanut-like shape, with smaller axis towards $M'$. 

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FIG. 1. 1-Fe and 2-Fe unit cells in (a) real and (b) momentum space. In (a) gray denotes Fe-atoms and purple denotes the Se-atoms puckered above and below the Fe-plane. The rotated red square denotes the 1-Fe unit cell, while the blue square denotes the 2-Fe unit cell. In (b) the corresponding unit-cells in momentum space are shown with schematic Fermi surfaces overlaid. In the 1-Fe unit cell (red), one electron pocket is centered at both $X$ and $Y$. In the 2-Fe unit cell (blue), there are two electron pockets at $M$ and two at $M'$ (note that the use of $M' = (-\pi, \pi)$ is not standard). In both unit cells, two hole pockets are centered at $\Gamma$.

(larger axis towards $M$).

The change of the shapes of the hole and electron pockets can be well understood at the mean-field level, by adding to the kinetic energy the fermionic bilinears that couple directly to the nematic order parameters:

$$
\mathcal{H}_{\text{nem}}^C = \phi_T \hat{d}^\dagger_{xz,\sigma} \hat{d}_{xz,\sigma} - \hat{d}^\dagger_{yz,\sigma} \hat{d}_{yz,\sigma} \\
\mathcal{H}_{\text{nem}}^M = \phi_1 (\hat{d}^\dagger_{xz,\sigma} \hat{d}_{xz,\sigma} - \hat{d}^\dagger_{yz,\sigma} \hat{d}_{yz,\sigma}) + \phi_3 (\hat{d}^\dagger_{xy,\sigma} \hat{d}_{xy,\sigma} - \hat{d}^\dagger_{yz,\sigma} \hat{d}_{yz,\sigma}).
$$

Here $\phi_T$ and $\phi_1$ are the nematic orders associated with the $xz$ and $yz$ orbitals near $\Gamma$ and $M$, respectively, and $\phi_3$ is the nematic order associated with the two $xy$ orbitals near $M$. We use $\hat{d}$ for the states at $\Gamma$, $\hat{d}$ for the states at the $Y$ point in the 1-Fe BZ and $d$ for the states at the $X$ point. The elongation of the hole pocket along $\Gamma - M'$ and the peanut-like form of the electron pocket, with larger axis along $\Gamma - M$, are reproduced if $\phi_T > 0$ and $\phi_1 < 0$ (Refs. 26, 29, 31). We will use this convention throughout. It implies that the $xz$ orbital is the dominant one for the hole pocket, while the $yz$ orbital is the dominant one for the inner electron pocket.

The sign change between $\phi_T$ and $\phi_1$ is consistent with the theoretical reasoning that, for repulsive interactions, a spontaneous nematic order is possible only if it changes sign between hole and electron pockets [32], similarly to an $s^{+-}$ superconducting order. The $\phi_3$ term leads to a splitting of the two degenerate $xy$ orbitals from the $X$ and $Y$ pockets (see Fig. 2). This term does not affect the peanut-like shape (shown in Fig. 3) of the inner electron pocket [20] and will play only a secondary role in our analysis. The sign (and magnitude) of this term has not been verified in experiments. In renormalization group calculations [33] the sign is the same as of $\phi_1$.

While the shape of the pockets near $M$ can be well understood by including only the standard terms in Eq. (1), the ARPES data for the excitations right at the $M$ point cannot be straightforwardly explained within the “standard model” of Eq. (1). Specifically, above $T_{\text{nem}}$, the $yz$ and $xz$ states at $M$ form a doublet and are degenerate. Below $T_{\text{nem}}$ they split exactly by $2\phi_1$, according to Eq. (1) (see Fig. 3). ARPES measurements deep in the nematic state do detect two sharp excitations [16, 18, 23–27, 34], and a recent polarized ARPES study [26] provided strong evidence that these two states are indeed $xz$- and $yz$-dominated, by tracking them from the $M$ to the $\Gamma$ point. However, as $T$ increases towards $T_{\text{nem}}$, the two states do not merge and remain split even above $T_{\text{nem}}$ [16, 18, 23–27, 34]. In Ref. 26 it was speculated that the absence of merging may be a spurious feature due to thermal broadening, while in Refs. 16, 18, 23–26 and 31 it is argued that the splitting of the two modes above $T_{\text{nem}}$ is a physical feature. If this is indeed the case, the ARPES data at $M$ are inconsistent with the standard model of Eq. (1).

In this communication we argue that the ARPES data at the $M$ point can be explained if one includes SOC for the fermions near the electron pockets. In the presence of SOC, the excitations at $M$ are no longer orbital eigenstates. In the tetragonal phase this does not lead to drastic changes: the excitations still form two doubly degenerate states, such that the states in the doublet closer to the Fermi level are $xz$ and $yz$ with small admixtures of $xy$, while the states in the doublet farther from the Fermi level are $xy$, one with a small admixture of $xz$, the other with a small admixture of $yz$ (see Fig. 4). Our key finding is that below $T_{\text{nem}}$, where the double degeneracy is lost, an excitation from each doublet undergoes an orbital transmutation, i.e. its dominant orbital contribu-
of

xz

mains predominantly

splits into two levels. In this case, the upper one re-

yz

into two energy levels: the upper one remains predom-

Specifically, the doublet closer to the Fermi level splits

only the terms of Eq. (1) and the

(a)–(c) and

T > T

FIG. 3. Fermi surfaces and orbital weights at $T \ll T_{\text{nem}}$

(b)–(f) for the standard case in which

only the terms of Eq. (1) and the $xy$ hopping anisotropy are

in between the

xz

and

yz

T

results agree with Refs. 16, 18, 23, 25, 27, and 34, which followed these two excitations from $T \ll T_{\text{nem}}$ to $T > T_{\text{nem}}$

T > T

We believe that this theoretical scenario solves the puzzle of ARPES data at the $M$ point in FeSe. As we said before, all ARPES experiments observe two sharp excitations at $M$ at $T \ll T_{\text{nem}}$ [16, 18, 23–27, 34]. Our results agree with Refs. 16, 18, 23, 25, 27, and 34, which followed these two excitations from $T \ll T_{\text{nem}}$ to $T > T_{\text{nem}}$

T > T

and argued that they remain split at $T > T_{\text{nem}}$. Our results also agree with Ref. 23 which identified two additional, less coherent excitations at $T \ll T_{\text{nem}}$, located in between the $xz$ and $yz$ dominated excitations. In our scenario, these excitations are identified as having predominantly $xy$ orbital character.

We also discuss the orbital composition of the pockets. The polarized ARPES and STM measurements show that the nematic order drastically changes the orbital content of the pockets deep in the nematic phase. In one domain the elliptical hole pocket becomes predominantly $xz$, and the inner electron pocket becomes predominantly $yz$. This is in sharp contrast to the behavior in the tetragonal phase, where the orbital content of these pockets oscillates between $xz$ and $yz$ (see Fig. 3). Such a drastic change of the orbital content is not expected in a generic FeSC, where $\phi_F$ and $\phi_1$ are much smaller than the corresponding Fermi energies $E_F$, but has been reproduced theoretically for FeSe [29, 30], where the pockets are smaller than in other FeSCs, and $\phi_F$ and $\phi_1$ are comparable to $E_F$. For the same parameters, calculations show that the outer electron pocket becomes larger and more circular in the nematic phase [16, 22, 29, 36, 37], and its orbital content is predominantly $xy$ (see Fig. 3). In other words, all pockets become nearly mono-orbital deep in the nematic state: the hole pocket becomes $xz$ ($yz$), the inner electron pocket becomes $yz$ ($xz$), and the outer electron pocket becomes $xy$ (and, if the second, smaller hole pocket does not sink completely below the Fermi level, its orbital content becomes $yz$ ($xz$)).

The near-$xy$ composition of the outer electron pocket may explain why this pocket has not been detected in ARPES measurements. Namely, it has been argued in several papers [2, 36, 38, 40], that the $xy$ fermions are ei-
ther completely incoherent, or have only a small coherent spectral weight at low-energies \((Z_{xy} \ll 1)\), with the rest of the spectral weight transferred to higher energies. If this is the case, then the pocket made of \(xy\) fermions is almost invisible to ARPES, as the large incoherent background would mask any shallow peaks.

The rest of the paper is organized as follows. In Sec. III we introduce the low-energy model and describe in more detail the standard coupling to the nematic order parameter, the SOC for fermions near \(M\), and the SIH term. We set the parameters in the fermionic dispersion to match the observed forms of hole and electron pockets in the tetragonal and the nematic phases. In Sec. IV we discuss the orbital composition of the Fermi pockets and the excitations at \(M\) in the presence of SOC. In Sec. V we discuss the same in the presence of SIH. We discuss the results and present our conclusions in Sec. VI.

II. THE LOW-ENERGY MODEL

We work in the crystallographic 2-Fe BZ, in which the electron pockets at \(X\) and \(Y\) are folded onto the \(M\) (and \(M'\)) points, and form inner and outer electron pockets. To obtain the fermionic dispersion, we follow Ref. [10] and use a \(\mathbf{k} \cdot \mathbf{p}\)-expansion around the \(M\) point, which respects all the symmetries of a single FeSe layer. In the absence of SOC, the orbital states at the \(M\) point are pure \(xy\) orbitals. Since the space group of FeSe, \(P4/\text{nnm}\), is non-symmorphic, all irreducible representations at the \(M\) point are two-fold degenerate [10], in which case the excitations form doublets (quadruplets, if we include spin degeneracy). The doublet closest to the Fermi level consists entirely of the \(xy\) orbitals originating from the two inequivalent Fe sites in the 2-Fe BZ (the states near \(X\) and near \(Y\) in the 1-Fe BZ). A suitable basis for these doublets is:

\[
\Psi(\mathbf{k}) = \begin{pmatrix} \Psi_Y(\mathbf{k}) \\ \Psi_X(\mathbf{k}) \end{pmatrix},
\]

where

\[
\Psi_Y(\mathbf{k}) = \begin{pmatrix} d_{xz,\sigma}(\mathbf{k}) \\ d_{xy,\sigma}(\mathbf{k}) \end{pmatrix}, \quad \Psi_X(\mathbf{k}) = \begin{pmatrix} d_{yz,\sigma}(\mathbf{k}) \\ d_{xy,\sigma}(\mathbf{k}) \end{pmatrix},
\]

and \(\mathbf{k}\) is the deviation from \(M\). As in Eq. [1], we label the states which are associated with the \(X\) pocket in the 1-Fe BZ point by \(\hat{d}\). The kinetic energy term in this basis is:

\[
\mathcal{H}_{\text{kin}}(\mathbf{k}) = \begin{pmatrix} h_+(\mathbf{k}) & 0 \\ 0 & h_-(\mathbf{k}) \end{pmatrix},
\]

with

\[
h_{\pm}(\mathbf{k}) = \begin{pmatrix} \epsilon_1 + \frac{k^2}{2m_1} & \pm a_1 k_x k_y \\ \pm i v_{\pm}(\mathbf{k}) & \epsilon_3 + \frac{k^2}{2m_3} \pm a_3 k_x k_y \end{pmatrix} \otimes \sigma^0,
\]

where \(\sigma^0\) is \(2 \times 2\) identity matrix (we use \(\sigma\) to denote matrices in spin-space) and \(v_{\pm}(\mathbf{k})\) is a polynomial in \(k\):

\[
v_{\pm}(\mathbf{k}) = v(\pm k_x + k_y) + p_1(\pm k_x^2 + k_y^2) + p_2 k_x k_y (k_x \pm k_y).
\]

At the \(M\) point, \(\mathbf{k} = 0\), the Hamiltonian is diagonal

\[
h_+(0) = h_-(0) = \begin{pmatrix} \epsilon_1 & 0 \\ 0 & \epsilon_3 \end{pmatrix} \otimes \sigma^0,
\]

i.e., the eigenstates are pure orbital states. We assume that the onsite energies \(\epsilon_1\) and \(\epsilon_3\) are slowly-varying functions of temperature and use \(\epsilon_1(T) = \epsilon_{1,0} + 0.083 T\), \(\epsilon_3(T) = \epsilon_{3,0} + 0.083 T\), where \(\epsilon_{1,0} = -24.6\) meV and \(\epsilon_{3,0} = -32.0\) meV, to reproduce the ARPES data at \(M\) in the tetragonal phase [3, 15, 21, 22, 24, 41]. We use these values in Figs. 2 and 3 to obtain the variation of the excitations at \(M\) in the nematic phase within the standard model. We will adjust \(\epsilon_{1,0}\) and \(\epsilon_{3,0}\) slightly in the presence of SOC and SIH to maintain the peanut-like shape of the inner electron pocket. The exact values will be given in the appropriate sections, but the variation between cases is rather small, within 3 meV.

Away from the \(M\) point, the eigenstates are no longer pure orbital states. We use the parameters listed in Table [1] to reproduce the ARPES and STM data for the peanut-like inner electron pocket [2, 5, 15, 21, 22, 24, 41]. The standard coupling of fermions near the \(M\) point to the nematic order parameters \(\phi_1\) and \(\phi_3\) is given by Eq. (1). For our analysis it suffices to consider a mean-field temperature-dependence of \(\phi_1\) and \(\phi_3\):

\[
\phi_i(T) = \phi_{i,0} \sqrt{1 - T/T_{\text{nem}}},
\]

where \(T_{\text{nem}} = 90\) K. For definiteness, we set \(\phi_{1,0} = -24\) meV in all calculations, and use three different values of \(\phi_{3,0}\) (\(\phi_{3,0} = 0\) and \(\phi_{3,0} = \pm 10\) meV). We will see that the results do not depend substantially on the choice of \(\phi_{3,0}\).

The Fermi surfaces and the thermal evolution of the excitations at the \(M\)-point within this standard model are shown in Figs. 2 and 3. The shape of the inner pocket and its orbital composition are consistent with ARPES and STM data. The outer electron pocket has predominantly \(xy\) orbital character. Fermions on the \(xy\) orbital are likely incoherent [35, 39], which may explain why this pocket has not been observed in ARPES studies in the nematic phase.

We see from Fig. 2 that the excitations at \(M\) retain their orbital character in the nematic phase: two of the four modes are \(xy\), one is \(xz\), and one is \(yz\). The \(xz\) and \(yz\) excitations are split at \(T < T_{\text{nem}}\), but merge at \(T = T_{\text{nem}}\) and form a doublet at \(T > T_{\text{nem}}\) (the energies of the two \(xy\) modes merge into another doublet). As stated above, this is inconsistent with ARPES. It is argued in several papers [16, 18, 22, 24, 27, 44], that the excitations identified as \(xz\) and \(yz\) deep in the nematic state remain split at \(T = T_{\text{nem}}\). In the next Section we show that a new effect, dubbed orbital transmutation, emerges once we extend the standard model to include SOC, and the
evolution of the excitations in the model with SOC is fully consistent with ARPES data.

The form of the SOC at the M point has been analyzed in Ref. [10] using symmetry considerations. It was argued that SOC leads to an additional off-diagonal term in the Hamiltonian $\mathcal{H}_{\text{kin}}(\mathbf{k})$ in Eq. (4):

$$\mathcal{H}_{\text{SOC}} = \begin{pmatrix} 0 & \hat{h}_{\text{SOC}} \\ \hat{h}_{\text{SOC}}^\dagger & 0 \end{pmatrix},$$

(8)

where

$$\hat{h}_{\text{SOC}} = \frac{i}{2} \left[ \begin{pmatrix} 0 & 1 \\ 0 & 0 \end{pmatrix} \otimes \sigma^1 + \begin{pmatrix} 0 & 0 \\ 1 & 0 \end{pmatrix} \otimes \sigma^2 \right].$$

(9)

In terms of the operators at M this is

$$\mathcal{H}_{\text{SOC}} = \frac{i}{2} \lambda \hat{d}_{xz,\alpha}^\dagger \sigma_{\alpha\beta}^z \hat{d}_{xy,\beta} + \frac{i}{2} \lambda \hat{d}_{xy,\alpha}^\dagger \sigma_{\alpha\beta}^y \hat{d}_{yz,\beta} + \text{H.c.}.$$ (10)

In the 1-Fe BZ, this couples $xz$ fermions at Y with $xy$ fermions at X, and $yz$ fermions at X with $xy$ fermions at Y. We emphasize that the coupling in Eq. (10) is the only symmetry allowed momentum-independent SOC. Momentum-independent couplings between $\hat{d}_{xz,\sigma}$ and $\hat{d}_{xy,\sigma}$ or $\hat{d}_{yz,\sigma}$ and $\hat{d}_{xy,\sigma}$, i.e. between fermions from the same electron pocket in the 1-Fe BZ, are not allowed by symmetry [10]. Momentum-dependent SOC terms are allowed [10, 42], but these terms are expected to be small in FeSe because the relevant momenta are small.

The sum of the kinetic energy term and the SOC term is

$$\mathcal{H}_{\text{tot}}(\mathbf{k}) = \begin{pmatrix} \hat{h}_v(\mathbf{k}) & \hat{h}_{\text{SOC}} \\ \hat{h}_{\text{SOC}}^\dagger & \hat{h}_{\text{soc}}(\mathbf{k}) \end{pmatrix}.$$ (11)

In the presence of SOC, excitations in the tetragonal phase still form two doublets (two quadruplets if we include spin), but each eigenstate no longer has pure orbital character (see Fig. 4 at $T > T_{\text{nem}}$). The two states from the upper doublet are still dominated by the $xz$ and $yz$ orbitals, but each now has an admixture of the $xy$ orbitals. Similarly, the two states from the lower doublet are still primarily $xy$, but one has an admixture of $xz$ and the other of $yz$. In the next Section we analyze how these states evolve in the nematic phase.

The SOC in Eq. (8) is the bulk term, and its form is set by the symmetry of the $P4/nmm$ space group of the bulk. In Sec. IV we consider the special situation at the surface, as both ARPES and STM generally probe electrons near the surface. The glide-plane symmetry is broken at the surface, which allows additional coupling terms to be present. One can describe the effect of the SOC in terms of an effective electric field $\eta$, perpendicular to the surface [13, 44]. Such a field transforms as the $A_{2u}$ irreducible representation of the $P4/nmm$ space group at the zone center. Consequently, it couples to the fermionic bilinear at the M-point, $\hat{d}_{xz,\sigma}^\dagger \hat{d}_{yz,\sigma} + \text{H.c.}$, which also transforms as $A_{2u}$. As a result, the Hamiltonian for fermions at the surface acquires an additional term

$$\mathcal{H}_{\text{surf}} = \eta \hat{d}_{xz,\sigma}^\dagger \hat{d}_{yz,\sigma} + \text{H.c.}.$$ (12)

In the presence of such term, the $xz$ and $yz$ orbitals remain degenerate at the M point in the tetragonal phase, but the new eigenstates are $d_{\pm,\sigma} = (\hat{d}_{xz,\sigma} \pm \hat{d}_{yz,\sigma})/\sqrt{2}$. This hybridization term splits the $xz/yz$ doublet and gives rise to two distinct states with mixed $xz/yz$ character at M (see Fig. 4 at $T > T_{\text{nem}}$).

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| $\epsilon_{1,0}$ | $\epsilon_{3,0}$ | $v$ | $p_1$ | $p_2$ | $(2m_1)^{-1}$ | $(2m_3)^{-1}$ | $a_1$ | $a_2$ |
|---|---|---|---|---|---|---|---|---|
| $-24.6$ | $-32.0$ | $-122.90$ | $-137.22$ | $-11.67$ | $1.41$ | $186.11$ | $136.12$ | $-403.84$ |

TABLE I. Parameters used in the low-energy model listed in units of meV.
III. EXCITATIONS IN THE NEMATIC PHASE IN THE PRESENCE OF SOC

The full Hamiltonian at $M$ in the nematic phase is the sum of $\mathcal{H}_{\text{nem}}^M$ from Eq. (1) and $\mathcal{H}_{\text{tot}}(\mathbf{k})$ from Eq. (11). Because the atomic SOC only couples $d_{xz}$ with $d_{xy}$ and $d_{yz}$ with $d_{xy}$ the Hamiltonian matrix at the $M$ point decouples into four $2 \times 2$ matrices. Each matrix can be straightforwardly diagonalized. Consider, e.g., $d_{xz,\uparrow}$ and $d_{xy,\downarrow}$. The corresponding $2 \times 2$ matrix Hamiltonian is

$$\begin{pmatrix} \epsilon_1 + \phi_1 & \frac{1}{2} \lambda \\ -\frac{1}{2} \lambda & \epsilon_3 - \phi_3 \end{pmatrix}. \quad (13)$$

The eigen-energies are

$$E_{\pm} = \frac{1}{2} \left( \epsilon_1 + \epsilon_3 + \phi_1 - \phi_3 \pm \sqrt{\lambda^2 + (\epsilon_1 - \epsilon_3 + \phi_1 + \phi_3)^2} \right),$$

and the transformation to the diagonal basis is

$$a = \hat{d}_{xz,\uparrow} \cos \varphi - i \hat{d}_{xy,\downarrow} \sin \varphi,$$

$$b = \hat{d}_{xy,\downarrow} \cos \varphi - i \hat{d}_{xz,\uparrow} \sin \varphi, \quad (15)$$

where

$$\tan 2\varphi = -\frac{\lambda}{\epsilon_1 - \epsilon_3 + \phi_1 + \phi_3}. \quad (16)$$

Accordingly, $E_+$ is the energy of the a excitation while $E_-$ is the energy of the b excitation. In the absence of SOC and for $\phi_1, \phi_3 = 0$, we find $\varphi = 0$. In this case, $E_+ = \epsilon_1$, and the excitation is made exclusively by $xz$ fermions, while $E_- = \epsilon_3$ is made by $xy$ fermions. For finite SOC, the weight of the $xz$ component for the $a$ fermions is $\cos^2 \varphi$ and the weight of the $xy$ component is $\sin^2 \varphi$. For the $b$ fermions the situation is the opposite: $\cos^2 \varphi$ is the weight of the $xy$ component, while $\sin^2 \varphi$ is the weight of $xz$. In Fig. 5 we show the evolution of $\varphi$ with increasing the magnitude of $\phi_1, \phi_3$.

For $d_{yz,\uparrow}$ and $d_{xy,\downarrow}$ (or $d_{yz,\downarrow}$ and $d_{xy,\uparrow}$) the excitation energies are instead

$$E_{\pm} = \frac{1}{2} \left( \epsilon_1 + \epsilon_3 - \phi_1 + \phi_3 \pm \sqrt{\lambda^2 + (\epsilon_1 - \epsilon_3 - \phi_1 + \phi_3)^2} \right), \quad (17)$$

and the transformation to the band basis is

$$\tilde{a} = \hat{d}_{yz,\uparrow} \cos \tilde{\varphi} - i \hat{d}_{xy,\downarrow} \sin \tilde{\varphi},$$

$$\tilde{b} = \hat{d}_{xy,\downarrow} \cos \tilde{\varphi} + i \hat{d}_{yz,\uparrow} \sin \tilde{\varphi}, \quad (18)$$

with

$$\tan 2\tilde{\varphi} = -\frac{\lambda}{\epsilon_1 - \epsilon_3 - \phi_1 + \phi_3}. \quad (19)$$

In this case, the weight of the $yz$ orbital for the $a$ excitation (the one with energy $E_+$) is $\cos^2 \tilde{\varphi}$, while the weight of $xy$ is $\sin^2 \tilde{\varphi}$. For the $b$ excitation the weight of $xy$ is $\cos^2 \tilde{\varphi}$, and the weight of $yz$ is $\sin^2 \tilde{\varphi}$.

The key to the phenomenon of orbital transmutation is the fact that in FeSe the difference $\epsilon_1 - \epsilon_3$ is smaller than in other Fe-based materials (recall $\epsilon_3 < \epsilon_1 < 0$). At some $T$ below $T_{\text{nem}}$, the combined value of the nematic order parameter $\phi_1 + \phi_3$, $\phi_1 + \phi_3 = -|\phi_1| + \phi_3$, is larger in magnitude than $\epsilon_1 - \epsilon_3$ (recall $\phi_1 < 0$ by assumption) [45]. This can actually be seen from Fig. 2: the $xz$ band, whose energy is $\epsilon_1 + \phi_1$ in the absence of SOC, crosses both $xy$ excitations, whose energies are $\epsilon_3 \pm \phi_3$. At low $T$, $\epsilon_1 - \epsilon_3 + \phi_1 + \phi_3$ therefore changes sign and becomes negative. This implies that $\varphi$, given by Eq. (16), varies from $\varphi \approx -0$ to $\varphi \approx \frac{\pi}{2}$. Accordingly, the content of the $a$ excitation at $E_+$ varies from near-$xz$ at $T > T_{\text{nem}}$ to near-$xy$ at $T < T_{\text{nem}}$. Similarly, the content of the $b$ excitation varies from near-$xy$ in the high-temperature regime to near-$xz$ deep in the nematic phase (see Fig. 5). For the $a$ and $b$ excitations no orbital transmutation occurs because $\epsilon_1 - \epsilon_3 - \phi_1 + \phi_3$ in the denominator of Eq. (19) does not change sign.

In Fig. 6 we show the results of the full calculation of the excitation spectrum for three values of $\phi_3$ (positive, negative, and zero). The boxes near the lines show the orbital content. We see that one branch of the split upper doublet remains predominantly $yz$ between $T = T_{\text{nem}}$ and $T < T_{\text{nem}}$, but the other becomes predominantly $xy$ instead of $xz$. For the lower doublet one branch remains predominantly $xy$, but the other becomes $xz$ instead of $xy$. Combining this with the assumption that the $xy$ orbital is incoherent [35, 39], we find that, deep in the nematic state, ARPES should see the sharp coherent $xz$ and $yz$ orbital states, (the latter closer to the Fermi level) and two much weaker incoherent $xy$ excitations in between these two. In Figs. 6 and 7 we show the spectral
function,
\[ A(k, \omega) = -2\text{Tr} \left[ \Im (\omega + i\Gamma - \mathcal{H}(k))^{-1} \right], \] (20)
both away and at the Fermi level. Here \( \mathcal{H}(k) \) is the full Hamiltonian including the nematic order, and \( \Gamma \) is a phenomenological diagonal damping term, which we assume to be larger for the \( xy \) orbital, to mimic its incoherence.

The results for the dispersions and the spectral functions in Fig. 6 are largely consistent with the available photoemission data. The two stronger peaks at \( T \ll T_{\text{nem}} \) have been identified by all photoemission groups [16–18, 22, 23, 25–27, 34]. Ref. 26 identified the orbital content of the excitation closer to the Fermi level as \( yz \) and the one farther from the Fermi level as \( xz \), by tracking these two excitations between the \( M \) and \( \Gamma \) points. Ref. 23 reported the observation of two weaker peaks in between the two stronger peaks. In our theory, these are the two \( xy \) excitations. As \( T \) increases towards \( T_{\text{nem}} \), the \( yz \) excitation evolves such that it becomes a component of the upper doublet at \( T > T_{\text{nem}} \), while the orbital character of the predominantly \( xz \) excitation at \( T \ll T_{\text{nem}} \) evolves as \( T \) is increased towards \( T_{\text{nem}} \) and becomes increasingly \( xy \) dominated. Thus, the \( yz \) and \( xz \) dominated excitations at \( T \ll T_{\text{nem}} \) do not merge at \( T_{\text{nem}} \) (see Fig. 4). Instead, the lower component of the upper doublet, which is predominantly \( xz \) for \( T \geq T_{\text{nem}} \) becomes predominantly \( xy \) as \( T \ll T_{\text{nem}} \) and hence becomes increasingly incoherent. ARPES data did indeed find that near \( T_{\text{nem}} \), the excitation closer to the Fermi level is sharper than the one farther from the Fermi level [3].

We also emphasize that the energy splitting of the \( xz \) and \( yz \) states at low \( T \) is not simply \( \Delta E = -2\phi_1 \), as it
would be without SOC, but

$$\Delta E = -\phi_1 + \phi_3 + \frac{1}{2} \sqrt{\lambda^2 + (\epsilon_1 - \epsilon_3 - \phi_1 - \phi_3)^2}$$

$$+ \frac{1}{2} \sqrt{\lambda^2 + (\epsilon_1 - \epsilon_3 + \phi_1 + \phi_3)^2};$$  \hspace{1cm} (21)

which is valid in the case $|\phi_1 + \phi_3| > |\epsilon_1 - \epsilon_3|$. The modified splitting is a direct consequence of the orbital transmutation. In Fig. 7 we show the two electron Fermi surfaces in the presence of SOC and the orbital composition of the pockets. We see that the smaller, peanut-shaped inner electron pocket is mainly made out of $yz$ fermions, while the outer, more circular-looking pocket is predominantly made out of $xy$ fermions. The peanut-shaped pocket does contain some admixture of both $xy$ and $xz$ along the diagonal direction. The $xz$ contribution is due to SOC. Because of its presence, this portion of the peanut-shaped pocket becomes visible to ARPES in the polarization orthogonal to $yz$, even if the $xy$ orbital is localized and not detectable. This agrees with Refs. 24 and 34, in which the portions of the peanut-shaped electron-pocket along the diagonal direction have been observed in the polarization orthogonal to $yz$. Note that the degree of $xz$ spectral weight along the diagonal direction is rather sensitive to the magnitudes of the SOC and the nematic order parameters.

In Fig. 8 we show the evolution of the dispersions along the direction from $M$ to $\Gamma$ at low $T \ll T_{nem}$ and at $T > T_{nem}$. We clearly see that along the $M - \Gamma$ direction, the orbital composition of the band that crosses the Fermi surface closer to $M$ changes drastically between $T > T_{nem}$ and $T \ll T_{nem}$. Orbital transmutation is much weaker along the orthogonal direction, where the main effect of the nematicity is the shrinking of the Fermi momentum for the $yz$ band along the shorter axis of the peanut-shaped Fermi surface.

FIG. 8. Dispersion along $M - \Gamma$ direction at $T \ll T_{nem}$ (a) and $T > T_{nem}$ (c) with the temperature evolution shown in (b). The key effect of nematicity is the drastic change of the orbital composition of the band that crosses the Fermi surface closer to $M$. The orbital color code is the same as in Fig. 2

In Fig. 9 we show the temperature evolution of the energies at the $M$-point in the case when the $xz$ and the $yz$ orbitals hybridize due to surface effects. The orbital color code is the same as in Fig. 2. Here $\epsilon_{1,0} = -26.3$ and $\epsilon_{3,0} = -32.0$ and we chose $\eta = 10$ meV. The doublet with $xz/yz$ orbital character is split by a surface-induced hybridization already at temperatures $T > T_{nem}$. As nematic order sets in at $T = T_{nem}$, the $yz$ orbital becomes more dominant in the state whose energy is closest to the Fermi level, while $xz$ is dominant for the state whose energy is farthest from the Fermi level, as seen by the difference between the colored bars at high and low temperatures. Note that the surface does not break the $xz/yz$ degeneracy above $T_{nem}$, and the split levels contain equal weights of the $xz$ and the $yz$ orbitals.

FIG. 9. Temperature evolution of the energies at the $M$-point in the case when the $xz$ and the $yz$ orbitals hybridize due to surface effects. The orbital color code is the same as in Fig. 2. Here $\epsilon_{1,0} = -26.3$ and $\epsilon_{3,0} = -32.0$ and we chose $\eta = 10$ meV. The doublet with $xz/yz$ orbital character is split by a surface-induced hybridization already at temperatures $T > T_{nem}$. As nematic order sets in at $T = T_{nem}$, the $yz$ orbital becomes more dominant in the state whose energy is closest to the Fermi level, while $xz$ is dominant for the state whose energy is farthest from the Fermi level, as seen by the difference between the colored bars at high and low temperatures. Note that the surface does not break the $xz/yz$ degeneracy above $T_{nem}$, and the split levels contain equal weights of the $xz$ and the $yz$ orbitals.

IV. EXCITATIONS IN THE NEMATIC PHASE IN THE PRESENCE OF SURFACE-INDUCED HYBRIDIZATION

In this Section we analyze separately the effect of the surface-induced hybridization (SIH), i.e., of the extra term in the Hamiltonian, given by Eq. (12). This term, allowed in the surface only, hybridizes fermions in the $xz$ and $yz$ orbitals at $M$ already in the tetragonal phase, where it splits the $xz/yz$ doublet into two distinct excitations with mixed $xz+yz$ and $xz-yz$ orbital character (see Fig. 9).
FIG. 10. Spectral function as function of $T$ and $\omega$ in the presence of the surface-induced hybridization term. The two peaks are clearly distinguished above the nematic transition and each can be traced all the way down to $T = 0$ K. The two shallow peaks, originating from the $xy$ modes, are at $\omega \approx -20$ and $\omega \approx -40$ meV at $T = 0$.

Below $T_{\text{nem}}$, the upper excitation shifts closer to the Fermi level, and its orbital content changes from an equal mixture of $xz$ and $yz$ to almost pure $yz$. The lower excitation shifts farther from the Fermi level, and its orbital content changes to almost pure $xz$. At low $T$, the two energies are split by $\Delta E = 2\sqrt{\varphi^2 + \eta^2}$. As $T$ increases towards $T_{\text{nem}}$, the two excitations get closer to each other, but remain split by $\Delta E = 2\eta$ also above the nematic transition, at $T > T_{\text{nem}}$.

In Fig. 11 we show the spectral function in the presence of SIH. Like before, we set the damping rate to be larger for $xy$ fermions to mimic their incoherence. The behavior is quite similar to that in the case of SOC. The two differences are (i) the $xz$ excitation remains coherent at all $T$, and (ii) the $xz$ and $yz$ excitations do not merge even if we extrapolate their positions based only on the low $T$ results. The Fermi surfaces, shown in Fig. 11 along with the orbital weights, is also similar to the case of finite SOC. For temperatures far below $T_{\text{nem}}$, the inner pocket remains predominantly of $yz$ character and the outer pocket has predominantly $xy$ character.

V. DISCUSSION AND CONCLUSIONS

In this paper we analyzed the puzzling ARPES data on FeSe of the electron pockets at the $M = (\pi, \pi)$ point. Deep in the nematic phase, at $T \ll T_{\text{nem}}$, ARPES experiments have detected two relatively sharp excitations at $M$ [16, 18, 23, 25–27, 34], and a recent study unambiguously identified these excitations as having predominantly $xz$ and $yz$ orbital character [26]. Above the nematic transition, at $T > T_{\text{nem}}$, the $xz$ and $yz$ orbital states are degenerate, and excitations associated with the $xz$ and $yz$ orbitals should therefore merge in the tetragonal phase. However, the data show that the two excitations come closer to each other, but remain split at $T > T_{\text{nem}}$. We argue that these results are reproduced if we include the effect of SOC.

In the presence of SOC, the excitations at $M$ form two doublets at $T > T_{\text{nem}}$. The upper doublet is predominantly made out of either the $xz$ or the $yz$ orbital, each with small admixtures of $xy$. The lower doublet consists...
We also argued that the larger electron pocket (the one but variation of $\eta$ only include SIH – our results are shown for tentatively the results do not change. The same holds if we orbital transmutation becomes more effective, but qualitatively the results do not change. The same holds if we variation of $\eta$ does not lead to qualitative changes. We also argued that the larger electron pocket (the one predominantly of $xy$ fermions, with small admixtures of either $xz$ or $yz$ fermions. Below $T_{\text{nem}}$, the components of each doublet are split, and there are four distinct excitations. We showed that the dominant orbital character of two of the excitations at $M$ changes drastically between $T > T_{\text{nem}}$ and $T \ll T_{\text{nem}}$. Namely, one of the excitations consisting predominantly of the $xy$ orbital along with a small admixture of $xz$ in the tetragonal phase, becomes near-$xz$ deep in the nematic phase. Similarly, the excitation dominated by the $xz$ orbital with a small admixture of $xy$ in the tetragonal phase, becomes near-$xy$ deep in the nematic phase. This phenomenon is due to an effect dubbed orbital transmutation. Because of this effect, the excitation dominated by the $xz$ orbital deep in the nematic phase changes orbital content to $xy$ as $T$ is increased towards $T_{\text{nem}}$, and ultimately merges with the lower doublet. As a result, the excitations dominated by the $xz$ and $yz$ orbitals at $T \ll T_{\text{nem}}$ do not merge at $T_{\text{nem}}$, in agreement with ARPES data. Other features of the spectral function at $M$, shown in Fig. 6 and the shape and orbital composition of the two electron pockets, shown in Fig. 4 also agree with the data. We showed that almost the same behavior is obtained if, instead of SOC, we include the SIH between the $xz$ and $yz$ orbitals at $M$. Such hybridization is not allowed in the bulk because it would violate the glide-plane symmetry, but is allowed at the surface. The only substantial difference between the effects of SOC and SIH is that, in the presence of SOC, there are two doublets at $T > T_{\text{nem}}$, while in the presence of SIH there is one $xy$ doublet $\eta=10\text{meV}$. Here $\epsilon_{1,0}=-27.6\text{meV}$ and $\epsilon_{3,0}=-32.0\text{meV}$. In this case, both doublets are split at $T > T_{\text{nem}}$. The $xz/yz$ doublet is split by the hybridization and the $xy$ doublet inherits this splitting through the SOC.

Neither SOC on the electron pockets, $\lambda$, nor the SIH, $\eta$, has been measured directly. For the hole pockets, SOC has been measured and is around 20 meV $\lambda$. We showed the results for $\lambda = 10\text{meV}$. As $\lambda$ increases, the orbital transmutation becomes more effective, but qualitatively the results do not change. The same holds if we only include SIH – our results are shown for $\eta = 10\text{meV}$, but variation of $\eta$ does not lead to qualitative changes. We also argued that the larger electron pocket (the one with non-peanut-like shape) is not seen in ARPES experiments because $xy$ fermions are incoherent.

The two scenarios can be distinguished by comparing measurements at the $M$ point in the tetragonal phase with measurements in the orthorhombic phase. In the SOC scenario, there are two doubly degenerate bands in the tetragonal phase, while in the SIH scenario there are four bands with different energies, compare Figs. 4 and
(recall that Fig. 9 assumes a vanishing SOC). Additionally, in the SOC scenario, one doubly degenerate band consists predominantly of the \(xz\) and \(yz\) orbitals, while the other is mostly \(xy\). If the \(xy\) orbital is more incoherent, the ARPES intensity of the \(xz/yz\) mode should be higher than the intensity of the \(xy\) mode, and the width of the first mode should be narrower. In the SIH scenario, two modes in the tetragonal phase are made equally of \(xz\) and \(yz\) orbitals, and their intensity should be equal, even if the other two modes (with \(xy\) character) are too incoherent to be detected. If both effects are present and are of comparable strength, ARPES measurements would reveal four peaks of varying intensity, depending on their relative orbital content (see Fig. 12).

A different reason for the disappearance of the second electron-pocket was put forward in Ref. 26. There, it was argued that it shrinks in the nematic phase. This is in variation with our result that the size of this pocket increases below \(T_{\text{nem}}\). The reduction of the non-peanut-shaped pocket can in principle be obtained if we assume that the magnitude of \(\phi_3\) is comparable to \(\epsilon_3\). However, this requires fine-tuning, and this scenario does not explain the non-merging of the \(xz\) and \(yz\) excitations at \(T_{\text{nem}}\).

Another seemingly appealing option is to introduce SOC or hybridization between \(xz/xy\) and \(yz/xy\) fermions within the same pocket in the 1-Fe BZ, i.e. add to the Hamiltonian the terms

\[
\mathcal{H}_{\text{intra-pocket hyb}} = \sum_{i} \left[ \eta_{\text{hyb}} (\hat{d}_{\alpha \beta i} \hat{d}_{\alpha \beta i}^\dagger + \text{H.c.}) + \lambda_{\text{hyb}} (\hat{d}_{\alpha i} \hat{d}_{\beta i}^\dagger \hat{d}_{\beta i} \hat{d}_{\alpha i}^\dagger + \text{H.c.}) \right],
\]

This would split the \(xz/yz\) and \(xy\) doublets and shrink the size of the non-peanut-shape pocket [26, 27]. However, we emphasize that neither Eq. (22) nor Eq. (23) are allowed by the \(P4/nmm\) space group symmetry, regardless of whether the system is in the tetragonal or in the nematic phase [10]. At the surface, \(\mathcal{H}_{\text{intra-pocket hyb}}\) is still not allowed, but \(\mathcal{H}_{\text{intra-pocket SOC}}\) with \(i = x, y\) is allowed [20]. However, this term is generated by the combination of atomic SOC, Eq. (10), and SIH, Eq. (12) and the effects of this term are secondary to those from the SOC and the SIH (see Figs. 12 and 13).

**ACKNOWLEDGMENTS**

We are grateful to Brian Andersen, Lara Benfatto, Anna Böhmer, Sergey Borisenko, Peter Hirschfeld, Jian Kang, Timur Kim, Andreas Kreisel, Dung-Hai Lee, Luke Rhodes, Matthew Watson, and Ming Yi for stimulating discussions. M.H.C. and R.M.F. were supported by the U.S. Department of Energy, Office of Science, Basic Energy Sciences, under Award No. DE-SC0012336. A.V.C. is supported by U.S. Department of Energy, Office of Science, Basic Energy Sciences, under Award No. DE-SC0014402.

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