Energy Balancing With Wide Range of Operation in the Isolated Multi-Modular Converter

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ABSTRACT
The series-connection of modules in multilevel converters are prone to energy imbalances in the dc capacitor due to the differences between the power absorbed and consumed. In renewable energy applications where the primary source is directly connected to each module, energy imbalances can be even worse if the primary sources are affected by unpredictable weather conditions. Therefore, control strategies are required to compensate such energy imbalances, while maintaining the correct converter operation. Focusing our attention on a cascaded transformer multilevel inverter called Isolated Multi-Modular Converter, this paper introduces the combination of two control strategies aimed at providing a wide range of operation under imbalanced energy states. A general analytical model, including the regulation capability and differences with an existing strategy are presented to demonstrate the performance of the control proposed. The effectiveness of the proposal is validated through experimental results based on a three-phase multilevel prototype.

INDEX TERMS
Cascaded transformer multilevel inverter, dc energy balancing, isolated multi-modular converter, multilevel converters.

I. INTRODUCTION
Cascaded multilevel converters based on H-bridge (CHB) configurations are among the most suitable multilevel topologies for large-scale photovoltaic (PV) power plants [1]–[4]. The series-connection of modules offers several advantages such as high-quality output voltage, reduced switching frequency and low harmonic distortion, among others. However, the use of multilevel converters for PV applications requires galvanic isolation because most commercial PV modules only tolerate voltage levels between 1000V and 1500V [5]. In order to provide such isolation, extra dc or ac stages are introduced. When galvanic isolation is provided on the dc side, a high-frequency transformer is mandatory in addition to a dc-dc converter. Therefore, maximum power point (MPP) can still be achieved on each PV string connected to the modules. Other multilevel configurations such as Modular Multilevel Converters (MMC) have also been proposed for PV applications [6], all of them based on dc-dc isolated stages.

Conversely, multilevel converters with galvanic isolation through low-frequency transformers have also gained more relevance in literature. Even though, they need bulky transformers, they are highly robust and reliable, important requirements for PV applications. Cascaded transformer multilevel inverters (CTMI) are some of these configurations [7]–[13]. They consist of several H-bridge modules connected in parallel to the same dc source, while the ac side is connected to low-frequency transformers. One of their main advantages is the possibility of setting a certain transformer ratio to reach symmetrical and asymmetrical voltage levels [14]–[16]. However, the limitation of using a single dc source in the case of large power applications has encouraged researchers to find other configurations such as the Isolated Multi-Modular Converter (IMMC) proposed in [17]. The IMMC has two arms in parallel with several modules connected to independent dc sources. Therefore, each PV string is isolated, opening the possibility for high power applications.
The power produced by PV panels is affected by non-uniform irradiance, temperature variations and partial shading. Therefore, if dedicated PV strings are connected to each module, a control strategy is required to operate under unbalanced power circumstances. For cascaded configurations, many control strategies have been proposed to balance the power mismatches between phases and modules of the same phase [18]–[22]. In [20] a control strategy aimed at operating under different power imbalances per phase has been proposed. The control strategy introduces a zero-sequence component in which each voltage reference is compensated according to its respective imbalance ratio. To deal with severe power imbalances, an optimal zero sequence injection is proposed in [21], but this strategy is only suitable for imbalances between phases. In order to control power imbalances between modules of the same phase, a capacitor voltage balancing is proposed in [22]. This strategy phase shifts the modulated voltage according to the dc voltage level. All these strategies have been validated in classical cascaded configurations, but not in the IMMC.

So far, power imbalances in the IMMC have been controlled based on the amplitude voltage compensation [17]. This control strategy was previously proposed for a cascaded H-Bridge multilevel converter in [22], [23] and for a cascaded T-Type configuration in [24]. However, its limited operating range does not allow large power imbalances. This is an important aspect to be considered, since a balance control strategy should have a strong regulatory capacity. Therefore, this paper proposes the combination of two control strategies to provide a wide range of power imbalance. The strategies are based on the amplitude voltage compensation introduced in [17] and on a proposed control strategy called quadrature voltage compensation which phase-shift the modulation index according to the power level of each module.

The rest of the paper is organized as follows: The operation principle of the IMMC and its central control architecture are reviewed in Section II. Then, the concept of power imbalances is described in Section III, where the amplitude and the quadrature voltage compensation are discussed. In section IV the combination of both control strategies are presented to demonstrate their high capability to withstand energy imbalances. Section V presents experimental results based on a three-phase configuration with 2 modules per arm to validate the effectiveness of the presented strategies working individually and combined. Finally, Section VI summarizes the work done.

II. OPERATION PRINCIPLE OF THE IMMC

The three-phase IMMC previously described in [17] is shown in Fig.1. The converter is formed by two arms per phase connected in parallel between a common point and a coupling inductance , which represents the equivalent inductance of a series-connection of low frequency transformers required to provide galvanic isolation. Each arm has modules formed by a 2-level voltage source converter and a low frequency transformers, where its primary side is connected to the inverter and the secondary side is connected to the next transformer. Thanks to this galvanic isolation, high floating voltages caused by the series-connection of modules are avoided, making the converter suitable for photovoltaic applications. Additionally, the series connection of modules increases the stepped voltage levels, reducing current harmonics while improving the power quality.

To understand the converter operation, the IMMC can be studied based on the dynamic model of both arms. Referring to each arm as upper and lower arm, from the nomenclature presented in Fig.1, the output and circulating current are given by:

\[
i_{o,k} = i_{u,k} - i_{l,k} \quad (1a)
\]

\[
i_{c,k} = \frac{i_{u,k} + i_{l,k}}{2} \quad (1b)
\]

The subscript \( u \) and \( l \) represent the upper and lower arm in phase \( k \), \( i_{o,k} \) is the output current and \( i_{c,k} \) is the circulating current flowing through the converter when there is an imbalanced energy operation.

Considering the fact that each module generates an output voltage \( v_{x,i} \) in the secondary side of the transformer, where \( x \) is the upper or lower arm and \( i \) represents the module, the voltage arm given by the series-connection of modules
per phase is reduced to:
\[
V_{s,k} = \sum_{i=1}^{N} v_{s,k,i}
\]  
(2)

Introducing the Kirchhoff’s voltage law in combination with the current and voltage expressions defined in (1) and (2), the dynamic model per phase of the IMMC is given by:
\[
\frac{R_T}{2} i_{o,k} + \frac{L_T}{2} \frac{d}{dt} i_{o,k} = v_{s,k} - v_{o,k}
\]
(3a)
\[
\frac{R_T}{2} i_{e,k} + \frac{L_T}{2} \frac{d}{dt} i_{e,k} = v_{c,k}
\]
(3b)
where \( L_T \) is the equivalent winding inductance defined by the low frequency transformers and \( R_T \) is the equivalent resistance used to model the arm losses. Note that two decoupled dynamic models have been declared to represent the output and circulating current behavior. In the case of the output current model, voltage \( v_{s,k} \) represents the voltage difference between the upper and lower arms. Similarly, in the circulating current model, voltage \( v_{c,k} \) is the average voltage arm, which also represents the voltage drop in the coupling inductance. These voltages can be described in terms of the voltage arms as follows:
\[
v_{s,k} = \frac{v_{l,k} - v_{a,k}}{2}
\]
(4a)
\[
v_{c,k} = \frac{v_{a,k} + v_{l,k}}{2}
\]
(4b)
These models can also be expressed in terms of the \( dq \) reference frame. Consequently, applying the Park transformation to equation (3), the dynamic models are expressed according to equations (5) and (6).
\[
\frac{R_T}{2} i_{od} + \frac{L_T}{2} \frac{d}{dt} i_{od} - jw_{oq}i_{od} = v_{ad} - v_{od}
\]
(5a)
\[
\frac{R_T}{2} i_{oq} + \frac{L_T}{2} \frac{d}{dt} i_{oq} + jw_{od}i_{oq} = v_{sq} - v_{oq}
\]
(5b)
\[
\frac{R_T}{2} i_{cd} + \frac{L_T}{2} \frac{d}{dt} i_{cd} - jw_{cd}i_{cd} = v_{cd}
\]
(6a)
\[
\frac{R_T}{2} i_{cq} + \frac{L_T}{2} \frac{d}{dt} i_{cq} + jw_{cq}i_{cq} = v_{cq}
\]
(6b)

A. INSTANTANEOUS POWER ANALYSIS

The energy operation of each module is closely related to the power flow between the primary source connected to the dc side and the active power delivered into the grid. Any power mismatch caused by a variation in the dc or ac side will create an energy imbalance which has to be compensated to allow a stable operation.

The energy analysis is carried out considering an average model per arm where the series-connection of modules is evaluated based on the ac voltage and current signals. Therefore, the active power in both arms are given by:
\[
p_{o,x} = \frac{3}{2} \Re \left[ (v_{ad} + jv_{aq})(i_{ad} - ji_{aq}) \right]
\]
\[
= \frac{3}{2} \Re \left[ (v_{ad} + jv_{aq})(\frac{i_{ad} - ji_{aq}}{2} + i_{cd} - ji_{cq}) \right]
\]
(7)
\[
p_{o,d} = \frac{3}{2} \Re \left[ (v_{ad} + jv_{aq})(i_{ad} - ji_{aq}) \right]
\]
\[
= \frac{3}{2} \Re \left[ (v_{ad} + jv_{aq})(\frac{i_{ad} - ji_{aq}}{2} + i_{cd} - ji_{cq}) \right]
\]
(8)
To observe the impact of the output and circulating currents on the active power, the current arms have been replaced according to equation (1) and decomposed into their \( dq \) components. A dependency of the output and circulating currents in both arms can be appreciated. This can also be seen when the total and the difference active powers are defined.
\[
p_T = \frac{3}{2} (v_{ad}i_{ad} + 2v_{cd}i_{cd}) + \frac{3}{2} (v_{od}i_{od} + 2v_{cq}i_{cq})
\]
(9)
\[
p_\Delta = \frac{3}{2} (v_{ad}i_{ad} - 2v_{cd}i_{cd}) + \frac{3}{2} (v_{od}i_{od} - 2v_{cq}i_{cq})
\]
(10)
According to (9) and (10), the total and the difference active powers represent the power delivered into the grid and the power imbalance between the upper and lower arms. Note how the \( d \) components of the output and circulating currents are associated to \( v_{ad} \) and \( v_{cd} \), while the \( q \) current components are related to the voltages \( v_{aq} \) and \( v_{cq} \).

It is assumed that the equivalent coupling inductances are quite small and, consequently, their voltage drops can be neglected. Therefore, the voltage arms are reduced to \( v_{udq} = -v_{odq} \) and \( v_{ldq} = v_{odq} \). Under this assumption, the total power is given by:
\[
p_T = -\frac{3}{2} (v_{ad}i_{ad} + v_{aq}i_{aq})
\]
(11)
Similarly, the power difference yields:
\[
p_\Delta = -\frac{3}{2} (v_{ad}i_{ad} + v_{aq}i_{aq})
\]
(12)

The definition of both active power components helps defining the dependency between the voltage and current signals required to set the appropriate references for the central control architecture of the IMMC.

B. CENTRAL CONTROL DESCRIPTION

As discussed in previous section, the total and the difference active powers are used to define the current references according to the total energy in the series-connection of modules. The relationship between the active power and the energy variation is given by the rate of energy change in the dc capacitor. According to [17], the rate of change is defined as:
\[
P_{o,x} = \frac{C_{sm}}{2N} \frac{d}{dt} \left( \frac{v_{dc,i}}{2} \right)^2
\]
(13)
where \( N \) is the number of modules per arm, \( C_{sm} \) is the dc capacitance and \( v_{dc,i} \) is the addition of all dc voltages per arm.

The dynamic model of the current arms and the rate of energy change in the dc capacitors can be used to define the control architecture oriented to regulate the average operation.
of the converter. The control architecture used in the IMMC includes two control loops as described below:

- The internal output and circulating current control loops based on PI controllers are required to provide a perfect tracking and avoid overcurrent levels.
- The external dc voltage control loops are required to define the output and circulating current references based on the total dc voltage and the rate of energy change provided by the series-connection of all modules per arm.

The control architecture shown in Fig. 2 has two external control loops to process the error between the reference and the measured dc voltages. Afterwards, the total and the difference active powers are multiplied by variables $K_T$ and $K_\Delta$ inferred from equations (11) and (12) to transform the power signals into the output and the circulating current references. A Phase-Locked-Loop (PLL) synchronizes the power signals into the output and the circulating current references. Likewise, the reactive power is related to the component of the output current reference.

The central control architecture defines the signals $\vec{v}_x$, $\vec{v}_c$, and $\vec{v}_s$ which according to (14) represent the $dq$ components of $\vec{v}_x$ and $\vec{v}_s$, respectively. Then, a decoupling stage based on (4) is used to obtain the average modulated voltages $\vec{v}_{ad}$ and $\vec{v}_{aq}$. Note that these signals do not differentiate between modules with higher or lower energy levels. This may result in instability issues, causing converter failures when the modules operate under energy imbalances. In order to solve this problem, a local control strategy has to be included to regulate the modulation index in accordance to the power and dc voltage levels.

$$\vec{v}_s = \begin{bmatrix} v_{sd} \\ v_{sq} \end{bmatrix}, \quad \vec{v}_c = \begin{bmatrix} v_{cd} \\ v_{cq} \end{bmatrix}, \quad \vec{v}_x = \begin{bmatrix} v_{sd} \\ v_{sq} \end{bmatrix}$$

### III. Amplitude and Quadrature Voltage Compensation

The series-connection of modules sets out several challenges to balance the energy and provides a stable state. Since each module is connected to independent dc sources, the probability of having different dc voltage levels is not low. Therefore, a control strategy to locally adapt the modulation index according to the dc voltage, allowing a certain range of energy imbalance is necessary.

So far, the central control architecture defines the average modulation index in all modules of the upper and lower arms. However, this control layer does not differentiate between modules with higher or lower energy levels, triggering to instabilities when modules generate difference power levels. As described in previous work [17], the energy balance is defined by the power exchange between the dc and ac side of one module, giving rise to:

$$P_{cx,i} = P_{dcx,i} - P_{ox,i}$$

where $P_{cx,i}$ is the absorbed or delivered power from the dc capacitor, $P_{dcx,i}$ is the dc power provided by the external source and $P_{ox,i}$ is the output power delivered into the grid. Note that the power from the dc capacitor is governed by the power difference between the external source and the ac grid, generating a positive value when $P_{ox,i} < P_{dcx,i}$ and a negative value when $P_{ox,i} > P_{dcx,i}$. Depending on the power sign, the dc voltage will increase or decrease due to the power expression described in (16).

$$P_{cx,i} = \frac{C_{sm}}{2} \frac{d}{dt} \left( v_{dcx,i}^2 \right)$$

The rate of energy change in the capacitor will increase the dc voltage when the power is positive and reduce it when the power is negative. Since the amount of energy is directly proportional to the quadratic dc voltage, a higher voltage level in the capacitor holds a higher energy. On the other hand, a lower dc voltage means a lower energy level. In order to regulate the amount of energy, it is necessary to control the power flow between the external source and the output power, so the dc voltage is set to a certain level. However, the dc source is affected by external conditions, which implies a higher uncertainty in its power production. Consequently, the energy balance can be regulated by using the output power, while the external dc source is considered as a perturbation. The output power in each module is given by:

$$P_{ox,i} = v_{xi,i} i_x \cos(\theta_{xi,i})$$

Equation (17) shows that the output power is affected by three different variables: the magnitude of the ac voltage,
the magnitude of the current arm and the phase angle between both signals. Owing to the current arm is a common variable in the series-connection of modules, the ac voltage and the phase angle are the only variables in each module capable of controlling the power flow individually. Therefore, the energy balance can be achieved by a local controller which adjusts the average modulation index considering either the amplitude ac voltage or its phase angle.

Based on this concept, the amplitude and quadrature voltage compensation strategies are described to withstand the energy imbalances.

A. CONTROL STRATEGY BASED ON AMPLITUDE VOLTAGE COMPENSATION

The amplitude voltage compensation has been previously described in [22]– [24]. This well-known control strategy modifies the modulated ac voltage $v_{x,i}$ amplitude in each module to adjust the active power flow and control the energy in the dc capacitor. To understand how the control strategy works, a vector analysis is presented in Fig.3. Vectors $v_{x,1}$, $v_{x,2}$, and $v_{x,3}$ represent the voltage state of three modules before adding the amplitude voltage compensation. By adding them up with the drop voltage of the coupling inductance, the output voltage $v_{o}$ is defined. Note that the current arm $i_x$ is shifted $\theta_i$ degrees in relation to the output voltage. This phase shift defines the direction of the drop voltage in $L_f$.

![Vector analysis of control strategy based on amplitude voltage compensation.](image)

After adding the amplitude voltage compensation, voltages $v_{x,1}$, $v_{x,2}$, and $v_{x,3}$ become $v'_{x,1}$, $v'_{x,2}$, and $v'_{x,3}$, respectively. Voltages $v'_{x,1}$ and $v'_{x,2}$ reduce their magnitude to reduce their output power, while $v'_{x,3}$ increases its magnitude to increase its output power, ensuring a complete balance operation. Since the amplitude voltage is linked to the $d$ component of the modulation index, the amplitude voltage compensation acts directly in the voltage arm $v_{id}$ given by the central control. Therefore, according to the control architecture of Fig.2, the local modulation index of each module after adding the voltage compensation yields:

$$\frac{2N}{v_{dc,x}^*} v_{id} + k_x \Delta m_{id,i} = m_{id,i}^*$$  \hspace{1cm} (18)

where $2N/v_{dc,x}^*$ is the constant required to normalize the control signal $v_{id}$ between $-1$ and $1$, $\Delta m_{id,i}$ is the compensation provided by the amplitude voltage control and $m_{id,i}^*$ is the new modulation index required to achieve the local voltage reference. The control architecture of the amplitude voltage compensation is illustrated in Fig.4.

![Control architecture of the amplitude voltage compensation.](image)

B. CONTROL STRATEGY BASED ON QUADRATURE VOLTAGE COMPENSATION

As previously stated, the output power of each module is commanded by the amplitude of the modulated voltage and its phase angle. In this second control strategy, the phase angle is used to phase shift the output voltage and regulates the energy level in the dc capacitor.

According to equations (7) and (8), the power arm is defined by the product between the current and voltage arms. Therefore, the output power per module in the $dq$ reference frame can be reduced to:

$$p_{ox,i} = \frac{3}{2} (v_{id,i} i_{id} + v_{sq,i} i_{sq})$$  \hspace{1cm} (19)

Voltage $v_{id}$ is associated to the voltage amplitude used to control the power flow in previous control strategy. On this occasion, voltage $v_{sq}$ causes the power regulation. However, this voltage will not have any effect on the energy regulation if the $q$ component of the current arm is zero. Since the current arm depends on the output and circulating currents, when no reactive power is produced, the output current $i_{sq}$ is zero. This creates a dependency on the $q$ component of the circulating current to control the power. As seen in the previous section, the central control architecture contains a droop gain $K_q$ for setting the circulating current reference $i_{eq}$.

Thus, the circulating current reference is given by:

$$i_{eq}^* = \Delta E_{max} \cdot K_q$$  \hspace{1cm} (20)

Energy $\Delta E_{max}$ defines the maximum energy difference between the series-connection of modules in one arm, while
the droop gain $K_q$ is defined according to the maximum circulating current allowed in the converter. A higher $i_{cq}$ generates a larger phase shift in the current arm. However, the limitation of this current component is defined by the maximum current allowed in the converter, which will contribute to adjust the phase angle as:

$$\theta'_i = \tan^{-1} \left( \frac{i_{cq}}{i_{xd}} \right) \tag{21}$$

After the circulating current $i_{cq}$ is defined, it is necessary to generate the proper output voltage $v_{xq,i}$ to control the power flow of each module. The vector analysis shown in Fig.5 describes the operation principle of the control strategy based on the phase angle, also known as quadrature voltage compensation.

![Vector analysis of control strategy based on quadrature voltage compensation.](image)

Before adding the quadrature voltage compensation, voltages $v_{x1}$, $v_{x2}$ and $v_{x3}$ represent the output voltage of three modules. By adding them up plus the drop voltage in the coupling inductance, the voltage $v_o$ modulated in the ac terminals is defined. Nevertheless, after adding the quadrature voltage compensation, the $q$ component of $v_{x,i}$ modifies the phase angle of each module while the circulating current $i_{cq}$ modifies $\theta_i$. Therefore, the output voltages become $v'_{x1}$, $v'_{x2}$ and $v'_{x3}$, while the local phase angles change to $\theta_1$, $\theta_2$ and $\theta_3$. The addition of $\theta_1$ and $\theta_2$ to the phase angle $\theta'_i$ reduces the power provided by modules 1 and 2, while the phase angle $\theta_3$ increases the power provided by module 3.

Similar to the analysis described in the amplitude voltage compensation, the modulation index given by the $q$ component of the voltage arm in the central controller after adding the quadrature voltage compensation is reduced to:

$$\frac{2N}{\sum i_{dx} v_{xq} + \Delta m_{xq,i}} = m^*_{xq,i} \tag{22}$$

Variable $v_{xq}$ is the $q$ voltage component brought about the central controller. $\Delta m_{xq,i}$ is the compensation required to adjust the dc voltage level and $m^*_{xq,i}$ is the new modulation index in module $i$. The control architecture of the quadrature voltage compensation is shown in Fig.6.

The voltage difference between the reference and the measurement signal is processed through a PI controller which sets the compensation of the average modulation index. Note that the circulating current sign is required to add or subtract the compensation from $m_{xq}$.

![Control architecture of the quadrature voltage compensation.](image)

**IV. COMBINATION OF BOTH CONTROL STRATEGIES**

The overmodulation defines the maximum operating range to withstand energy imbalances. Therefore, If the converter run close to the overmodulation level, the capability to tolerate imbalances will be small. This is one of the main drawbacks in the amplitude voltage compensation as it has a direct effect on the modulation index amplitude. On the other hand, the quadrature voltage compensation phase shifts the modulated voltage based on the circulating current $i_{cq}$. As a result, high levels of circulating currents may increase the capability to tolerate high energy imbalances but also the converter losses.

The combination of both control strategies can be used to withstand high levels of energy imbalances, reducing the circulating current by adjusting at the same time the amplitude and the phase angle of the modulated signals. In order to analyze the operating range of both control strategies, in Fig.7 is shown the modulation index response of one module operating under multiple power deviations. The analysis starts with three modules per arm producing the same power level. Then, the first module decreases its power to increase the power imbalance. Fig.7.a shows the modulation response of the IMMC based on the amplitude and quadrature voltage compensation working individually. In the case of the amplitude voltage compensation, a small power deviation triggers to a fast increase in the modulation index. The maximum power deviation achieved before overmodulation is 40%.

Using the quadrature voltage compensation, the capability to tolerate energy imbalances is higher than the amplitude voltage compensation. When the circulating current $i_{cq}$ is 25% the nominal current arm, the modulation index reaches the overmodulation at 45% of power. Nevertheless, as the circulating current increases, the control strategy is able to withstand larger energy imbalances. Note that a circulating current of 45% is capable to tolerate a power deviation of 75%.

However, implementing the amplitude and the quadrature voltage compensation together, the capability to withstand energy imbalances is even higher. Fig.7.b shows how a circulating current of 25% tolerates a 70% of power imbalance and a 100% of power imbalance with a circulating current of 45%.
The control architecture embedded in each module based on both control strategies is illustrated in Fig.8. The error between the voltage reference and the voltage measured is processed through both control loops. The amplitude voltage compensation regulates the $d$ component of the modulation index, while the quadrature voltage compensation regulates the $q$ component.

### V. EXPERIMENTAL RESULTS

In an attempt to clarify and validate the IMMC working under energy imbalances, a 4.8 kW prototype with two modules per arm is tested with both control strategies. In the first scenario, the amplitude and quadrature voltage compensation are individually evaluated, then the combination of both strategies are used to show the higher tolerance under energy imbalances. The laboratory setup and its electrical circuit diagram are shown in Fig.9. Two modules based on three-phase inverters are connected in series through the secondary winding of three-phase transformers. Additionally, an LC filter is used to mitigate high frequency components, reducing the ac current ripple. On the other hand, to emulate four independent PV panels, a programmable dc source (Magna-Power TSD1000-20/36) is connected in series to dc resistors, emulating the voltage range between the maximum power and open-circuit operation. The central and local controllers are implemented in control platforms based on DSPs TMS320F28335 from Texas Instrument. In the central control platform, the average dc voltage and the internal current control loops are evaluated. The local control platforms embedded in each converter cabinet are used to balance the energy, set physical signals and provide voltage and current protections. The status variables and control signals are transmitted through a bidirectional communication bus based on a CAN-open protocol.

The connection between the IMMC converter and the ac grid is performed through an auto-transformer to operate at $320 \text{ VLLRMS} / 50 \text{ Hz}$. All parameters are listed in Table 1.

In order to evaluate the maximum energy difference, dc voltage steps are set in the upper and lower arm modules. The voltage, current and power response are illustrated from Fig.10 to Fig.14.

### TABLE 1. Experimental parameters.

| Parameters                        | Symbol | Value  |
|-----------------------------------|--------|--------|
| Nominal Power                     | $P_n$  | 4.8kW  |
| Nominal Power per module          | $P_{z,i}$ | 1.2kW  |
| Grid Voltage                      | $v_g$  | 320V   |
| Grid Frequency                    | $f_g$  | 50Hz   |
| Number of modules per arm         | $N$    | 2      |
| dc-link Capacitance               | $C_{sm}$ | 4700$\mu$F |
| dc Resistor                       | $R_{dc,i}$ | 22.5$\Omega$ |
| Switching Frequency               | $f_s$  | 8200Hz |
| Open-circuit voltage              | $v_{op}$ | 440V   |
| MPP Voltage                       | $v_{mp}$ | 360V   |
| Inductance LC Filter              | $L_I$  | 3mH    |
| Capacitance LC Filter             | $C_I$  | 5$\mu$F |
| Transformer Voltage               | $V_T$  | 400V   |
| Transformer Power                 | $P_T$  | 2kW    |
| Transformer Inductance            | $L_{T_2}$ | 8.3$\mu$H |
compensation. In Fig.10.a, a dc voltage step is introduced in module $M_{u1}$ to operate the upper arm at different energy levels based on the amplitude voltage compensation. This change is conducted by increasing the dc voltage from 360V to 390V, giving rise to a power decrease of 390W. The new power level creates a power difference between the upper and lower arm, triggering to a circulating current flowing through the converter. Due to the fact that the amplitude voltage compensation set the $q$ component of the circulating current to 0, the difference between the upper and lower power arms is directly related to the current amplitude.

In Fig.11.a, the phase $\alpha$ of the current arms are illustrated before and after the voltage step is set in module $M_{u1}$. Owing to all modules operate at maximum power (1.2 kW), the current arms have the same amplitude but shifted 180°. However, after the dc voltage of module $M_{u1}$ increases to 390V, the upper current arm decreases as the circulating current increases. Remember that the amplitude voltage compensation has a direct effect on the modulation index amplitude, therefore, its control range is restricted by the overmodulation level.

After 3s, a second voltage step is introduced in the second module $M_{l2}$ of the lower arm. Fig.10.a illustrates how the dc voltage $v_{dd,2}$ increases from 360V to 390V, triggering to a power decrease of 390W. This second power step creates an energy imbalance between the modules, but since both arms generate the same power, no circulating current flows through the converter.

A similar scenario is conducted using the quadrature voltage compensation. However, due to the higher capability to tolerate energy imbalances, on this occasion a dc voltage step of 40V is introduced in the upper arm module $M_{u1}$ and a second voltage step of 60V is introduced in the lower arm module $M_{l2}$, as seen in Fig.10.b. To withstand these energy imbalances, a circulating current $i_{cq}$ of 35% the nominal current arm has been set. In Fig.11.b is illustrated how this circulating current component phase shifts the current arm after...
the dc voltage in $M_{u1}$ increases. Additionally, it is observed a reduction in the amplitude of the upper current arm due to the power decrease.

**B. IMBALANCED ENERGY OPERATION BASED ON THE COMBINATION OF THE AMPLITUDE AND QUADRATURE VOLTAGE COMPENSATION**

In previous study case, the amplitude and quadrature voltage compensation where individually evaluated, demonstrating that the quadrature voltage compensation provides a higher capability to tolerate energy imbalances. In this study case, the combination of both strategies are evaluated to increase even more the energy imbalance operation. Similar to the previous case, two dc voltage steps are introduced. However, the capability to handle larger energy imbalances allows bigger voltage steps. The results are described in Fig.12 and Fig.13.

Before the voltage steps, all modules operate at nominal power. After 3.5s, a voltage step of 40V is introduced in $M_{u1}$, increasing the dc voltage from 360V to 400V. Since both control strategies are used, a circulating current $i_{cd}$ equal to 35% the nominal current arm is set to withstand this energy imbalance. Fig.13 shows how the upper and lower current arms are phase shifted as the circulating current increases. Note that an intrinsic circulating current $i_{cd}$ arises, as a consequence of the current difference between the upper and lower arms.

Combining both control strategies, the voltage compensation adjusts the $d$ and $q$ components of the control signals at
the same time. In order to evaluate the higher capability to withstand energy imbalances, a second voltage step of 80V is introduced in $M_{12}$. This voltage creates a large power decrease in $M_{12}$. However, it can be seen how the converter is able to withstand such energy imbalance.

C. COMPARATIVE ANALYSIS BETWEEN BOTH CONTROL STRATEGIES

The power response of all previous scenarios are studied in Fig.14. The energy imbalance based on the amplitude voltage compensation allows a maximum power difference of 33% between the two modules connected in series. However, in the quadrature voltage compensation, the circulating current $i_{dq}$ introduced allows a power difference of 65% as seen in the second power step of Fig.14b. When combining both control strategies the operating range become significantly larger, allowing higher energy imbalances. In Fig.14c it is illustrated how the second voltage step decreases the power generated by module $M_{12}$ close to zero, creating a power difference of 100%.

VI. CONCLUSION

This paper has proposed the combination of two control strategies in the Isolated Multi-Modular Converter to withstand wide energy imbalances in the series connection of modules. The control strategies are embedded in each module and adjust the average modulation index provided by the central controller, which regulates the total energy per arm through two current control loops. The control strategy proposed regulates the amplitude and phase angle of the modulation index. The amplitude voltage compensation adjusts the $d$ component of the modulation index, while the quadrature voltage compensation adjusts the phase angle through the $q$ voltage component. Experimental results based on two modules per arm have validated the effectiveness and feasibility of the control proposed, demonstrating that the IMMC is able to withstand large levels of energy imbalances and operates even if some modules decrease their power to critical levels.

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