CLASP Constraints on the Magnetization and Geometrical Complexity of the Chromosphere-Corona Transition Region

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Abstract

The Chromospheric Lyman-Alpha Spectro-Polarimeter (CLASP) is a suborbital rocket experiment that on 2015 September 3 measured the linear polarization produced by scattering processes in the hydrogen Lyα line of the solar disk radiation. The line-center photons of this spectral line radiation mostly stem from the chromosphere-corona transition region (TR). These unprecedented spectropolarimetric observations revealed an interesting surprise, namely that there is practically no center-to-limb variation (CLV) in the Q/I line-center signals. Using an analytical model, we first show that the geometric complexity of the corrugated surface that delineates the TR has a crucial impact on the CLV of the Q/I and U/I line-center signals. Second, we introduce a statistical description of the solar atmosphere based on a 3D model derived from a state-of-the-art radiation magneto-hydrodynamic simulation. Each realization of the statistical ensemble is a 3D model characterized by a given degree of magnetization and corrugation of the TR, and for each such realization we solve the full 3D radiative transfer problem taking into account the impact of the CLASP instrument degradation on the calculated polarization signals. Finally, we apply the statistical inference method presented in a previous paper to show that the TR of the 3D model that produces the best agreement with the CLASP observations has a relatively weak magnetic field and a relatively high degree of corrugation. We emphasize that a suitable way to validate or refute numerical models of the upper solar chromosphere is by confronting calculations and observations of the scattering polarization in ultraviolet lines sensitive to the Hanle effect.

Key words: magnetic fields – polarization – Sun: transition region – Sun: UV radiation

1. Introduction

Recent theoretical investigations predicted that the hydrogen Lyα line of the solar disk radiation should be linearly polarized by the scattering of anisotropic radiation, with measurable polarization signals in both the core and wings of the line (Trujillo Bueno et al. 2011; Belluzzi et al. 2012; Štěpán et al. 2015). Moreover, such radiative transfer investigations pointed out that the line-center polarization is modified by the presence of magnetic fields in the chromosphere-corona transition region (TR) via the Hanle effect. These theoretical investigations motivated the development of the Chromospheric Lyman-Alpha Spectro-Polarimeter (CLASP), an international sounding rocket experiment that on 2015 September 3 successfully measured the wavelength variation of the intensity and linear polarization of the Lyα line in quiet regions of the solar disk (see Kano et al. 2017, and references therein to the papers describing the instrument). CLASP observed the Lyα Stokes profiles I, Q, and U with a spatial resolution of about 3 arcsec and a temporal resolution of 5 minutes. The resulting Q/I and U/I linear polarization signals are of order 0.1% in the line-center and up to a few percent in the nearby wings, both showing conspicuous spatial variations with scales of ~10 arcsec, in agreement with the theoretical predictions. However, the observed Q/I line-center signals do not show any clear center-to-limb variation (CLV; see Figure 1), in contrast with the results of the above-mentioned radiative transfer investigations in several models of the solar atmosphere. The observed lack of a clear CLV in the Q/I line-center signal came as an interesting surprise because many other solar spectral lines show such a variation (e.g., Stenflo et al. 1997), including the K line of Ca II whose line-center Q/I and U/I spatial variations are sensitive to the magnetic and thermal structure of the chromosphere at heights...
a few hundred kilometers below the TR (Holzreuter & Stenflo 2007).

The plasma of the upper solar chromosphere is highly structured and dynamic, departing radically from a horizontally homogeneous model atmosphere. In 3D models resulting from magnetohydrodynamic (MHD) simulations (e.g., Carlsson et al. 2016), the TR, where the temperature suddenly increases from about 10⁴ K to the 10⁶ K coronal values, is not a thin horizontal layer, but it delineates a highly corrugated surface. In this Letter, such corrugated surface is characterized by specifying, at each point, the vector \( \mathbf{n} \) indicating the direction of the local temperature gradient (hereafter, the local TR normal vector).

We begin by illustrating that the spatial variations of the line-center \( Q/I \) and \( U/I \) signals of the Lyα line are very sensitive to the geometric complexity of the corrugated surface that delineates the TR. Second, we demonstrate that the significant CLV of the \( Q/I \) line-center signal of the Lyα line calculated in Carlsson et al.’s (2016) 3D radiation MHD model of the solar atmosphere can be reduced by increasing the magnetic field strength and/or the geometrical complexity of the model’s TR. We then show how this can be exploited to constrain, from the CLASP line-center data, the magnetic strength and geometric complexity of the solar TR by applying the statistical inference method discussed in Štepánek et al. (2018). To this end, we confront the statistical properties of the CLASP line-center data with those of the polarization signals calculated in a grid of 3D model atmospheres characterized by different degrees of geometrical complexity and magnetization.

2. An Analytical Corrugated Transition Region Model

In a 1D model atmosphere, static or with radial velocities, unmagnetized or with a magnetic field having a random azimuth at sub-resolution scales, the radiation field at each point within the medium has axial symmetry around the vertical. We take a reference system with the Z-axis (i.e., the quantization axis) along the vertical, and choose the reference direction for linear polarization perpendicular to the plane formed by the vertical and the line of sight (LOS; i.e., the parallel to the limb). In this reference system and under such circumstances, \( U/I = 0 \), and the following approximate formula can be applied to estimate the line-center \( Q/I \) scattering polarization signal of the hydrogen Lyα line (Trujillo Bueno et al. 2011):

\[
\frac{Q}{I} \approx \frac{1}{2\sqrt{2}}(1 - \mu^2)\mathcal{H} \frac{J^2_0}{J^2},
\]

where \( \mu = \cos \theta \) (with \( \theta \) the heliocentric angle), \( \mathcal{H} \) is the Hanle depolarization factor (\( \mathcal{H} = 1 \) for \( B = 0 \) G and \( \mathcal{H} < 1 \) in the presence of a magnetic field), and \( J^2_0/J^2 \) is the degree of anisotropy of the spectral line radiation at the height in the model atmosphere where the line-center optical depth is unity along the LOS (see Equations (2) and (3) of Trujillo Bueno et al. 2011). As seen in Figure 1 of Trujillo Bueno et al. (2011), the anisotropy factor of the hydrogen Lyα line suddenly becomes significant at the atmospheric height where the line-center optical depth is unity, which practically coincides with the location of the model’s chromosphere-corona TR. Therefore, under such assumptions, we should expect a clear CLV in the \( Q/I \) line-center signal, established by the \( (1 - \mu^2) \) factor of Equation (1), and modified by the height-dependence of the anisotropy factor (see the height range between the two solid-line arrows in Figure 1 of Trujillo Bueno et al. 2011). Because of our choice for the reference direction for linear polarization, the only way to have \( U/I \neq 0 \) in such a 1D model atmosphere is by means of the Hanle effect of a magnetic field inclined with respect to the local vertical. However, in such a 1D model atmosphere there is no way to destroy the CLV of the \( Q/I \) line-center signal.
The line-center photons of the hydrogen Lyα line originate just at the boundary of the model’s TR. In a 1D model atmosphere (e.g., Fontenla et al. 1993), the vector normal to the TR lies along the vertical, which coincides with the symmetry axis of the incident radiation field. In a 3D model atmosphere (e.g., Carlsson et al. 2016), the model’s TR delineates a corrugated surface, so that the vector normal to the model’s TR changes its direction from point to point (see Figure 7 of Štepán et al. 2015). On the other hand, at each point on such corrugated surface the stratification of the physical quantities along the local normal vector \( \mathbf{n} \) is much more important than along the perpendicular direction. In order to estimate how the line-center fractional polarization of the hydrogen Lyα line is at each point of the field of view, it is reasonable to assume that the incident radiation field has axial symmetry around the direction of the normal vector \( \mathbf{n} \) corresponding to the spatial point under consideration (see also Štepán et al. 2018). Taking a reference system with the \( Z \)-axis directed along the normal vector \( \mathbf{n} \), and recalling Equation (1), at each point of the corrugated TR surface we can estimate the line-center fractional polarization signals through the following formula:

\[
\frac{Q}{I} \approx \frac{1}{2\sqrt{2}} (1 - \mu_n^2) H \left[ \frac{J_0}{J_0} \right]_{m,n},
\]

where the positive Stokes \( Q \) reference direction is now the perpendicular to the plane formed by \( \mathbf{n} \) and the LOS, \( \mu_n \) is the cosine of the angle between \( \mathbf{n} \) and the LOS, and \( \left[ \frac{J_0}{J_0} \right]_{m,n} \) is the anisotropy factor calculated in the new reference system. Clearly, because the direction of \( \mathbf{n} \) changes as we move through the corrugated surface that delineates the TR, the \( Q/I \) signals estimated with Equation (2) do not share the same reference direction for the quantification of the linear polarization. In order to arrive at equations for \( Q/I \) and \( U/I \) having the parallel to the nearest limb as the positive Stokes \( Q \) reference direction, we have applied suitable rotations of the reference system. Specifying the direction of the local TR normal vector through its inclination \( \theta_n \) with respect to the vertical (with \( \theta_n \) between 0° and 90°) and azimuth \( \chi_n \) (with \( \chi_n \) between 0° and 360°), our analytical calculations show that the line-center \( Q/I \) and \( U/I \) signals of the hydrogen Lyα line can be estimated by the following formulas:

\[
\frac{Q}{I} \approx \frac{1}{2\sqrt{2}} \left[ \sin^2 \theta (3 \cos^2 \theta_n - 1) \right]
\]

\[
- \sin \theta \cos \theta \sin \theta_n \cos \theta_n \cos \chi_n
\]

\[
+ \frac{1}{4} (1 + \cos^2 \theta) \sin^2 \theta_n \cos (2\chi_n)
\]

\[
\left[ \frac{J_0}{J_0} \right]_{m,n},
\]

\[
\frac{U}{I} \approx \frac{1}{2\sqrt{2}} \left[ \cos \theta \sin^2 \theta_n \sin (2\chi_n) \right]
\]

\[
- \sin \theta \sin \theta_n \cos \theta_n \sin \chi_n \left[ \frac{J_0}{J_0} \right]_{m,n},
\]

3. The Impact of the Magnetization and Geometrical Complexity in 3D Models

The analytical TR model described in the previous section is very useful for understanding why the spatial variations of the \( Q/I \) and \( U/I \) line-center signals of the Lyα line are very sensitive to the geometry of the corrugated surface that delineates the solar TR. The magnetic field of such an analytical model is characterized by a random azimuth at sub-resolution scales, which implies that the impact of the model’s magnetic field strength on the CLV is just the scaling factor \( H \) that appears in Equations (3) and (4). We now show theoretical results for the 3D radiation MHD model of the chromosphere-corona TR of Carlsson et al. (2016), which is representative of an enhanced network region and has magnetic field lines reaching chromospheric and coronal heights.

The first two rows of Figure 3 show examples of the CLV of the \( Q/I \) and \( U/I \) line-center signals calculated with the radiative transfer code PORTA (Štepán & Trujillo Bueno 2013) in the 3D model of Carlsson et al. (2016) ignoring (first row) and taking into account (second row) the CLASP instrument degradation (see Giono et al. 2016 for information on the PSF). Clearly, the peak-to-peak amplitudes of the \( Q/I \) and \( U/I \) variations are significantly smaller when the degradation produced by the instrument is accounted for. Note that the \( Q/I \) line-center signals calculated in such a 3D model show a clear CLV.

The panels in the third row of Figure 3 show what happens when the magnetic field strength at each point in the 3D model is increased by a scaling factor \( \beta = 8 \), so that the mean field strength at the model’s TR is 120 G instead of 15 G. Clearly, an enhanced magnetization in the TR plasma has a significant impact on the linear polarization amplitudes, but it does not destroy the CLV of the \( Q/I \) line-center signal.

We show now what happens when the geometric complexity of the TR of the 3D model is modified. To this end, we simply compress the horizontal extension of the 3D model by a factor \( \gamma \) along the X and Y directions, so that the divergence of the model’s magnetic field vector at each grid point remains equal to zero and its modulus unaltered. The panels in the bottom row of Figure 3 provide an example for \( \beta = 1 \) (i.e., the model’s magnetic field), but with \( \gamma = 1/4 \). Clearly, the degree of corrugation of the model’s TR surface has an important impact on the CLV of the line-center \( Q/I \) signals.

4. Constraining the Degree of Magnetization and Corrugation of the Solar TR

We aim at constraining the magnetic field strength and degree of corrugation of the TR corresponding to the solar disk regions observed by CLASP. To this end, we confront the \( Q/I \) and \( U/I \) line-center signals measured by CLASP (hereafter, \( S^{\text{obs}} \)), with the theoretical line-center signals \( S \) calculated in a
grid of 3D models characterized by the scaling factors $\beta$ and $\gamma$, with $\beta = \gamma = 1$ corresponding to the 3D model described in Carlsson et al. (2016). Each pixel along the 400 arcsec spectrograph slit image corresponds to a particular LOS, and we have considered those having $\mu$ values between 0.1 and 0.8, with the exception of the faint filament region located around $\mu = 0.7$ in Figure 1. The theoretical $I$, $Q$, and $U$ profiles have been degraded to mimic the CLASP resolution according to the laboratory measurements described in Giono et al. (2016).

To determine the 3D model whose emergent $Q/I$ and $U/I$ line-center signals are the closest to those observed by CLASP, we apply the statistical inference approach discussed in Section 3.1 of Štěpán et al. (2018), which gives the following expression for the posterior of the hyper-parameters $\theta$ (i.e., the corrugation parameter $\gamma$ and the magnetization parameter $\beta$) based on the line-center data at all the CLASP spatial pixels $i$:

$$p(\theta | S^{\text{obs}}) = \prod_i \mathcal{L}_i(\theta | S^{\text{obs}}) p(\theta) = \mathcal{L}(\theta | S^{\text{obs}}) p(\theta),$$

Figure 2. CLV of the Stokes $Q/I$ (left) and $U/I$ (right) line-center signals of the hydrogen Ly$\alpha$ line calculated according to Equations (3) and (4) with $\beta = 1$ (no magnetic field) and $[R^2/R^3]_0 = -0.02$, for the fixed inclinations ($\theta_n$) of the TR normal vector $\mathbf{n}$ indicated in the panel insets and assuming random azimuths $\chi_n$. Note that the bottom panel corresponds to the case in which $\theta_n$ also has random values (see the text for details). The reference direction for the positive Stokes $Q$ is the parallel to the nearest limb.
where \( p(\Theta) \) is the prior of the hyper-parameters. The likelihood
\[ L_i(\Theta | S^{\text{obs}}) \]
with \( \sigma^2 \) the variance of the uncorrelated Gaussian noise. We point
out that \( p^\mu(S|\Theta) \) are the hierarchical priors of \( S \) that depend on
the hyper-parameters \( \Theta \). This is derived from the histograms of the
\( S \) signals calculated for each \( \mu_i \) value in each particular 3D
model characterized by its scaling factors \( \beta \) and \( \gamma \). In the CLASP
observations the standard deviation of the noise is \( \sigma = 0.05\% 
\) after averaging three pixels in wavelength around the line-center.

Our prior for the corrugation of the TR is that any
compression of the 3D model is allowed, while expansions
are much less likely (i.e., \( p(\gamma) = 1/2 \) for \( \gamma \in [0, 1] \) and \( p(\gamma) = \exp(-((\gamma - 1))/2 \) for \( \gamma > 1 \)). For the magnetic field
strength of the TR of the quiet Sun we have deemed it
reasonable to use \( p(B) = \exp(-B/130)/130 \), based on the
argument that the mean field strength of the quiet regions of the
solar photosphere is of the order of 100 G and that it decreases
with height in the atmosphere (Trujillo Bueno et al. 2004). This
is our first step for determining the parametrization \( \Theta \) of the
abovementioned 3D statistical model of the solar atmosphere
that maximizes the marginal posterior of Equation (5). Our aim
is to estimate some global properties of the quiet Sun

Figure 3. CLV of the Stokes \( Q/I \) (left) and \( U/I \) (right) line-center signals of the hydrogen Ly\( \alpha \) line calculated in the 3D model of Carlsson et al. (2016), ignoring
(topmost panels) and accounting for (rest of the panels) the degradation produced by the CLASP instrument. The panels of the first and second rows show the results
corresponding to the magnetic field and TR corrugation of the original 3D model. Those of the third row show the results obtained assuming an enhanced
magnetization characterized by a scaling factor \( \beta = 8 \) (which implies a mean field strength of 120 G in the model’s TR). The panels of the fourth row show the results
obtained assuming a compression factor \( \gamma = 1/4 \) (which quantifies the geometrical complexity of the model’s TR). The red curves in the left panels are best fits
quadratic in \( \mu \) to the fluctuating spatial variations. The reference direction for the positive Stokes Q is the parallel to the nearest limb.
5. Conclusions

Our statistical approach to interpret the spectropolarimetric observations of the hydrogen Lyα line achieved by CLASP suggests that the mean field strength of the TR than in the model of Carlsson et al. (2016) produce scattering polarization signals that are in better agreement with those observed by CLASP. A more robust conclusion is that, among the magnetized models needed to explain the CLASP observations, 3D models with a significantly larger degree of corrugation of the TR would yield a better agreement with the observations.

We think that our conclusion on the geometric complexity of the TR plasma is more robust than the one on its degree of magnetization because in order to cancel completely the CLV of the Q/I line-center signals we need to increase the degree of corrugation of the model’s TR, while the information on its magnetic strength is mainly encoded in the peak-to-peak amplitudes of the Q/I and U/I spatial radial variations, which are sensitive to the CLASP PSF used (based on laboratory measurements) and to the 3D model atmosphere chosen for the statistical inference. In any case, a key point to emphasize is that the linear polarization produced by scattering processes in the core of the hydrogen Lyα line encodes valuable information on the magnetic field and geometrical complexity of the chromosphere-corona TR, which can be revealed with the help of statistical inference methods such as the approach applied in this Letter. Clearly, having simultaneous spectropolarimetric observations in two or more spectral lines would facilitate the determination of the plasma magnetization, especially if the main difference between the spectral lines used lies within their sensitivity regime to the Hanle effect.

It is evident that we need more realistic 3D numerical models of the upper chromosphere of the quiet Sun. Chromospheric spicules are ubiquitous in subarcsecond-resolution Lyα filtergrams (Vourlidas et al. 2010), but they are not present in Carlsson et al.’s (2016) model. Our investigation suggests that 3D models with such needle-like plasma structures all over the field of view would be a much better representation of the geometric complexity of the TR plasma observed by CLASP. Finally, it is also important to emphasize that a suitable way to validate or refute numerical models of the chromosphere-corona TR is by confronting calculations and observations of the scattering polarization in ultraviolet lines sensitive to the Hanle effect. We plan to pursue further this line of research by also exploiting the polarization observed by CLASP in the resonance line of Si III at 1206 Å (see Ishikawa et al. 2017) and, of course, the observations of the Mg II h and k lines that the future flight of CLASP-2 will provide.

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