Constrained Local UniversE Simulations: A Local Group Factory

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ABSTRACT
Near field cosmology is practiced by studying the Local Group (LG) and its neighbourhood. The present paper describes a framework for simulating the “near field” on the computer. Assuming the ΛCDM model as a prior and applying the Bayesian tools of the Wiener filter (WF) and constrained realizations of Gaussian fields to the Cosmicflows-2 (CF2) survey of peculiar velocities, constrained simulations of our cosmic environment are performed. The aim of these simulations is to reproduce the LG and its local environment. Our main result is that the LG is likely a robust outcome of the ΛCDM scenario when subjected to the constraint derived from CF2 data, emerging in an environment akin to the observed one. Three levels of criteria are used to define the simulated LGs. At the base level, pairs of halos must obey specific isolation, mass and separation criteria. At the second level the orbital angular momentum and energy are constrained and on the third one the phase of the orbit is constrained. Out of the 300 constrained simulations 146 LGs obey the first set of criteria, 51 the second and 6 the third. The robustness of our LG ‘factory’ enables the construction of a large ensemble of simulated LGs. Suitable candidates for high resolution hydrodynamical simulations of the LG can be drawn from this ensemble, which can be used to perform comprehensive studies of the formation of the LG.

Key words: methods:N-body simulations – galaxies: haloes – cosmology: theory – dark matter

1 INTRODUCTION
These are exciting times for cosmology. Observations of the anisotropies of the cosmic microwave background (CMB) radiation by the WMAP and Planck observatories have provided spectacular validation of the standard model of cosmology, the ΛCDM. Observations of distant objects, spanning a look-back time of over 12 Gyrs, provide further support for the ΛCDM predictions for the growth of structure in the universe. The basic tenets of the model consist of an early inflationary phase, a prolonged phase a homogeneous and isotropic expansion dominated by the dark matter (DM) and dark energy, and structure that emerges out of a primordial perturbation field via gravitational instability.

Cosmology is the science of the biggest possible generalization. It deals with the Universe as a whole. This leads to an inherent tension between the drive, on the hand, to study the general properties of everything that we observe and, on the other, the wish to study the particularities of our own patch of the Universe. It follows that cosmology can be practiced by observing the Universe on the largest possible scales. But it can be practiced also by observing the very ‘local’ universe, resulting in the so-called near field cosmology (Bland-Hawthorn & Peebles 2006; Bland-Hawthorn & Freeman 2014). Near field cosmology can test some of the predictions of the ΛCDM model, and indeed possible conflicts have been uncovered. Locally observed dwarf and satellite galaxies seem to be at odd with predictions based on cosmological galaxy formation simulations (e.g. Peebles & Nusser 2010; Oman et al. 2015 and references therein). It is this tension between cosmology, practiced...
at large, and the near-field cosmology which motivates the Constrained Local UniversE Simulations (CLUES) project in general and the present paper in particular. Our aim here is to present a numerical laboratory which enables the testing of the near field cosmology against cosmological simulations.

The modus operandi of standard cosmological simulations is that they are designed to represent a typical and random realization of the Universe within a given computational box. Indeed, cosmological simulations have been the leading research tool in cosmology and the formation of the large scale structure (LSS). Near field cosmology poses a challenge to the standard cosmological simulations - how to associate environs and objects from the random simulations with our own Local Group (LG) and its environment? Bayesian reconstruction methods and constrained simulations provide an alternative to standard cosmological simulations. The basic idea behind these methods is the use of a Bayesian inference methodology to construct constrained realizations of the local universe of either the present epoch or initial conditions for numerical simulations. These constrained realizations are designed to obey a set of observational data and an assumed theoretical prior model. Two main streams have been followed - one uses galaxy peculiar velocity surveys and the other galaxy redshift surveys. Ganon & Hoffman (1993) were the first to generate constrained initial conditions from peculiar velocity surveys, and these were used by Kolatt et al. (1996) to run the first constrained simulations of the local universe. This early work has been extended by the CLUES project, within which many velocity constrained simulations have been performed (Gottloeber et al. 2010; Yepes et al. 2014 and references therein). Bistolas & Hoffman (1998) and later Mathis et al. (2002) ran the first redshift survey constrained simulations of the local universe, based on the IRAS survey (Davis et al. 1991). The application of Bayesian quasi-linear Hamiltonian Markov Chain Monte Carlo sampling methods to galaxy redshift surveys has provided a new and interesting way to reconstruct the local universe (see e.g. Kitaura et al. 2010, Jasche et al. 2010, Wang et al. 2014, Ata et al. 2015, Lavaux & Jasche 2016). Yet, these methods have a limited scope of resolution of a few megaparsecs and therefore are unable to resolve the LG itself. Presently the only available constrained simulations of the LG are the ones conducted by the CLUES project, to be described below.

In the case of the old CLUES simulations (i.e. the ones reported in Yepes et al. 2014), the underlying methodology gives raise to only a small number of "realistic" (numerical) LGs - ones with mass, distance and relative velocities akin to the observed LG. In fact, roughly 200 constrained simulations yielded only 4 acceptable LG candidates. Though the smallness of the sample hindered a statistically systematic study of the LG within the LCDM cosmology, performing high resolution zoom simulations of two of them it has nonetheless been possible to address a large number of relevant cosmological and astrophysical issues, such as the universality of the DM halo profiles (Di Cintio et al. 2013), properties of substructure (Libeskind et al. 2010), local implications of the Warm Dark Matter paradigm (Libeskind et al. 2013a) and peculiarities of the mass aggregation history of the LG (Forero-Romero et al. 2011).

One of the major aims of the CLUES project is to turn it into a 'factory' that produces on demand LG-like simulated objects, allowing for a systematic study of the properties of the LG - within the framework of the LCDM model and the Cosmicflows-2 data base of peculiar velocities (CF2; Tully et al. 2013) see the discussion below). The present paper shows how the incorporation of the CF2 new data and the improved methodology have turned the CLUES project into an efficient 'factory' that produces LGs, essentially on demand.

The basic pillar of the CLUES approach rests on the fact that in the standard model of cosmology the primordial perturbation field constitutes a Gaussian random field. The Bayesian linear tools of the Wiener filter (WF) and the constrained realisations (CRs) of Gaussian fields enable the construction of ICs constrained both by a given observational data base and an assumed prior model (Hoffman & Ribak 1991; Zaroubi et al. 1995). It follows that there are two attractors that 'pull' the ICs - the prior (cosmological) model and the observational data. Where - either in configuration or in the resolution (k) space - the data is strong the ICs reproduce the constraints, and otherwise they correspond to random realizations of the prior model. To the extent that 'strong' data is used as constraints the resulting ICs are likely to reproduce the observed local universe. The so-called constrained variance of the constrained realizations is significantly smaller than the cosmic variance of the prior model. Consequently, the reduction in the cosmic variance measures the 'strength' of the data, for the given prior model.

The improvement in the CLUES constrained simulations has proceeded along two main streams. In the methodological one the original WF/CR algorithm has been amended by the application of the Reverse Zeldovich Approximation (RZA) (Doumler et al. 2013a,b,c; Sorce et al. 2014) technique, which accounts for the Zeldovich displacement of the data points. On the data stream, the CF2 (Tully et al. 2013) database of galaxy peculiar velocities, corrected for the Malmquist bias by the method described by Sorce (2015), is used to constrain the ICs. Sorce et al. (2016) recently presented this new generation CLUES simulations. The present paper extends it to the case of zoom simulations of the LG.

The work starts with Section 2, that explains the basic ideas behind the Constrained Simulation (CS) method and its numerical implementation. Section 3 describes the Local Universe, listing the properties which will be used as a benchmark for the quality of the reconstruction, while Section 4 discusses the design of the simulations in relation to the aims of the present study. Then, Section 5 is devoted to the analysis of the reconstructed Local Neighbourhood: The Local Void, the local filament and the Virgo cluster. Section 6 contains a discussion on the identification and the properties of LG-like pairs, showing that in spite of the large role played by the random short-wave modes a substantial number of candidates can be identified using distinct classification criteria. In Section 7 the results are summarized and the plan of the future applications of this method is sketched.

2 CONSTRUED SIMULATIONS

At the very core of the constrained simulations lies the WF/RZA/CR method. Its main features will be briefly reviewed in the following subsections, addressing the interested reader to the original works for a comprehensive theoretical review.

2.1 Methods

The WF is a powerful tool for reconstructing a continuous (Gaussian) field from a sparse dataset, assuming a prior model. Its use in cosmology has been pioneered by Rybicki & Press (1992) while Zaroubi et al. (1995) first applied the method to the reconstruction of fields from observational dataset. In practice, the WF recon-
struc
tion results in an estimate of the true underlying field which is dominated by the data in the region where the sampling is dense while reproducing the priors where the data is lacking or uncertain due to large observational errors. The recovered velocity field is then easily converted into the cosmic displacement field, which in turn is used to trace back the object to its progenitor’s position. The latter is called the RZA procedure, which shifts backwards the observed radial component of the velocity only. The RZA can be improved replacing the radial constraints at these positions by the full three dimensional WF estimation of the velocity field’s components (Sorce et al. 2014).

However, the recovered velocity field will tend to zero in the regions where data is lacking or dominated by the error, since the WF will tend towards the mean field, which is the assumed prior. This can be compensated by means of the Constrained Realisation algorithm (CR) (Hoffman & Ribak 1991), that basically fills the data-poor regions with a random Gaussian field while converging to the constraints’ values where these are present, also ensuring the overall compliance with the prior’s power spectrum. This means that the outcome of a simulation will be determined by the interplay between these random modes and the constraints. In particular, the additional random components will play a role in two separate regimes: 1) The very large scales, where the data is sparse and error dominated and 2) the very small scales, which are dominated by the intrinsic non-linearity of the processes involved and cannot be constrained by the RZA. In our case, understanding of the latter kind of randomness is crucial, since it is dominant on the scales that affect the formation of LG-like objects.

2.2 Numerical implementation

The constrained white noise fields are generated using the techniques described by Doumler et al. (2013a,b,c); Sorce et al. (2014) on 256$^3$ nodes grids, which represent the minimum scale on which the constraints are effective (Sorce et al. 2016). Short-wave $k$-modes can be added to the input white noise field using the Ginnungagap[1] numerical package.

This numerical setup, that combines two different codes, turns out to be extremely relevant to our study, since (as anticipated) one will have to deal with two sources of randomness, i.e. the one coming from the constrained white noise field, affecting the data-poor large scales, and the small scale one, introduced by Ginnungagap when increasing the mass resolution. This is why, among the other reasons that are explained later, we chose to design and study different sets of simulations that separately relied on the two codes, exploiting their different capabilities in different ways and thus allowing us to spot any numerics-induced effect on the results.

3 THE LOCAL UNIVERSE

Our definition of the Local Universe encompasses two separate sets of objects; one is the Local Neighbourhood, which we define as the ensemble of the largest structures around the MW, and the other is the Local Group itself. Even though our main goal is the simultaneous reproduction of both of them, the differences in scales and methods to be used demands a step-by-step separate treatment. In what follows, a general description of these objects will be provided, with the aim of establishing a benchmark to gauge the quality of the reconstruction method at different scales and resolutions.

### 3.1 The Local Neighbourhood

Around the supergalactic coordinates (−3.1, 11.3, −0.58)h$^{-1}$ Mpc is located Virgo, the closest cluster of galaxies, whose estimated virial mass exceeds $4 \times 10^{14} h^{-1}$ $M_{\odot}$ (Tully et al. 2009) and is part of the much larger Laniakea supercluster (Tully et al. 2014). Virgo is the most massive object in our neighbourhood, and the effects of its gravitational pull can be observed even at the level of the Local Group. Since MW and M31 both live in a filament (Klypin et al. 2003; Libeskind et al. 2015) that stretches from it to the Fornax cluster.

The main properties of this Local Filament are derived! by analysing the eigenvectors of the (observational) velocity shear tensor around the LG position, which can be recovered from the CF2 dataset (Tully et al. 2013). The CF2 is a catalog of more than 8000 galaxy distances and peculiar velocities, which have to be further grouped to smooth out the small scale non-linearities, reducing the final number of constraints to less than 5000 points, and treated in order to minimize the biases (Sorce 2015).

Table 1. Eigenvector coordinates and eigenvalues at the LG position for the velocity shear tensor, taken from Libeskind et al. (2015). Since eigenvectors are non-directional lines, the $+/−$ directions are arbitrary.

| $\hat{e}_1$ | $\hat{e}_2$ | $\hat{e}_3$ |
|---|---|---|
| SGX | SGY | SGZ | $\lambda$ |
| −0.331 | −0.318 | 0.881 | 0.148 |
| 0.788 | 0.423 | 0.446 | 0.051 |
| 0.517 | −0.848 | −0.110 | −0.160 |

Fig. 1 shows the WF reaction applied to the CF2 data, plotting three density slices of $\pm 25h^{-1}$ Mpc side and $\pm 5h^{-1}$ Mpc thickness centered around the LG position, showing both the velocity streams and overdensity contours; a similar reconstruction was obtained by (Courtois et al. 2013) using the CF1 dataset. This image clearly depicts the nature of the large scale flows in our neighbourhood; for instance, in the supergalactic $X − Y$ plane it can be seen the flow moving from the center of the box towards Virgo, along the local filament, which then points in the direction of the Great Attractor (not shown) towards the negative $X$. In the $X − Z$ and $Y − Z$ planes, instead, the effect of the local void can be seen in the $Z > 0$ quadrant, where the velocity streams clearly indicate an outward movement from such a region.

The local void was first detected and described by Tully & Fisher (1987); however, its nature and extension are still uncertain so that estimations of its diameter range from 20 Mpc (Nasonova & Karachentsev 2011) to > 45 Mpc (Tully et al. 2008). It is this large underdense region, situated in the proximity of the LG, which is responsible for the observed peculiar velocities of galaxies in its vicinity, including MW and M31 (Tully et al. 2008). Libeskind et al. (2015) also showed that the center of the local void is aligned with $\hat{e}_1$ (the eigenvector associated with the largest eigenvalue), its numerical value is shown in Table 1, the direction that defines the strongest infall of matter, again showing the strong influence of this region on the dynamics in the neighbourhood of the MW.

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2 https://github.com/ginnungagapgroup/ginnungagap
of around Cen A, a group of galaxies located at a distance and their satellites form a relatively isolated system, the largest (van der Marel & Guhathakurta 2008, while MW and M31

The MW and M31 thin planes centered around either of the two hosts (Lynden-Bell 1976; Pawlowski et al. 2013; Ibata et al. 2013). The MW and M31 masses are consistent with van der Marel et al. (2012), Boylan-Kolchin et al. (2013).

Table 2. Kinematic properties of MW and M31 in the MW frame of reference. Distances and errors from van der Marel & Guhathakurta (2008), while MW and M31 masses are consistent with van der Marel et al. (2012), Boylan-Kolchin et al. (2013).

| Parameter | Unit   | Value          |
|-----------|--------|----------------|
| $r_{M31}$ | kpc    | 770 ± 40       |
| $r_{M31}$ | kpc    | (378.9, 612.7, −283.1) |
| $\sigma_{r,M31}$ | kpc | (18.9, 30.6, 14.5) |
| $v_{M31}$ | km s$^{-1}$ | (66.1, −76.3, 45.1) |
| $\sigma_{V,M31}$ | km s$^{-1}$ | (26.7, 19.0, 26.5) |
| $V_{M31,tan}$ | km s$^{-1}$ | < 34.4 |
| $V_{M31,rad}$ | km s$^{-1}$ | −109.3 ± 4.4 |
| $M_{200,tot}$ | $10^{12} h^{-1} M_\odot$ | 3.14 ± 0.58 |
| $M_{200,MW}$ | $10^{12} h^{-1} M_\odot$ | 1.6 ± 0.5 |
| $M_{200,M31}$ | $10^{12} h^{-1} M_\odot$ | 1.6 ± 0.5 |

3.2 The Local Group

The term Local Group refers to the group of galaxies dominated by M31 and MW. There are more than 70 additional galaxies belonging to it, most of whom are of dwarf type and are co-rotating around thin planes centered around either of the two hosts (Lynden-Bell 1976; Pawlowski et al. 2013; Ibata et al. 2013). The MW and M31 and their satellites form a relatively isolated system, the largest closest object being Cen A, a group of galaxies located at a distance of around 2.7 $h^{-1}$ Mpc. Table 2 shows the kinematic properties of the LG’s main players, from which it can be noticed a substantial uncertainty on the mass of the system and a stark difference between the tangential and radial components of the system’s velocity. In particular, the latter property makes the LG an outlier from the dynamical point of view, since a factor of three difference between these two components in halo pairs of this size is very rarely observed in cosmological simulations (Fattahi et al. 2015).

4 THE SIMULATIONS

The simulation of the Local Universe is a complex task that passes throughout several phases, due to the variety of the techniques involved and to the different nature (large scale and small scale) of the objects to be simulated. The present section motivates the choice of the design of the simulations in relation to the different aims of the present paper, with a particular emphasis on the intrinsic limitations of the CS method.

4.1 Aims

The properties of the MW and M31 satellites, namely their number and anisotropic distribution, have deep implications for the ΛCDM model itself (Klypin et al. 1999; Kroupa et al. 2005) and is hence one of the strongest motivations for the study of the nearby Universe. Even though these phenomena cannot be constrained directly, the CS framework provides a powerful and robust pipeline to reproduce the environment in which the LG forms, which is an element that might help explaining the peculiarities of MW and M31 (González et al. 2014).

In the context of simulations, this means that one has to disentangle the randomness of the short-wave modes from the large scale constrains and to gauge the effectiveness of CSs and their variance.

Since the reconstruction of the environment is itself a non-trivial task, unaffected by what happens at LG scales, we decide to take a two steps approach. This way one can ensure that larger structures such as Virgo are well recovered without first bothering about what happens to the LG, which is way more problematic due to the predominance of random modes. If this is the case, i.e. the reconstructed local neighbourhood compares well to the observational benchmarks previously outlined, one can at least hope for a successful outcome at smaller scales if some deeper relation between the LG and its environment exists.

In practice, to do this one has to run two series of simulations, addressing different (but related) questions, namely:

- how stable are the properties of the local neighbourhood? Which role does the random component of the CR plays on these scales?
- how many LG-like objects can be obtained at the expected position? How can they be properly defined and characterized?

In the first case it is clear that there is no need for high resolution, since a sufficiently large number of simulations is enough in order to address the question of the stability of the results and to estimate the constrained variance of the CS method in the quasilinear regime. Even though the CS produces stable results when using boxes of side 500 $h^{-1}$ Mpc, as shown by Sorce et al. (2016), smaller simulation volumes deserve a separate analysis. In fact,
when dealing with sub-Megaparsec scales it is necessary to deal with the issues of mass resolution (which needs to be high in order to reliably identify MW and M31-sized haloes) and sample variance (which demands to perform a very large number of simulations). This trade-off can be minimized by the use of zoom-in techniques. In order to do this while answering to the questions above, we have designed three series of simulations, which will be described in the following subsection.

4.2 Settings

In Table 3 are shown the parameter settings for the Initial Conditions (ICs) of the three series of simulations. The size of the box has been chosen as a compromise between the need for resolution and the necessity to minimize the effects of periodic boundary conditions on Virgo and the local filament. All of the simulations are run using the following cosmological parameters: \( \Omega_m = 0.312, \Omega_{\Lambda} = 0.688, h = 0.677 \) and \( \sigma_8 = 0.807 \) which are compatible with the Planck-I results (Planck Collaboration et al. 2013). To minimize boundary effects and maximize the power of the constraints, the observer is placed at the center of the box: This will be considered our expected LG position, around which candidate pairs will be searched for.

This means that the question about LG-like structures has to be addressed by a different type of simulations. The approach in this case has been that of adding a sufficiently large region around the box center with an equivalent resolution of \( 6.57 \times 10^8 h^{-1} \text{M}_\odot \), which allow to identify this kind of objects with \( \approx 10^3 \) Dark Matter (DM) particles. This is enough to ensure their stability in the process of increasing the resolution by adding further levels of mass refinement. The size of this first zoom-in region has been chosen as follows. For each SimuLN256 run, all the particles within a sphere of \( R \approx 5 h^{-1} \text{Mpc} \) around the box center (the expected LG location) at \( z = 0 \) were taken and traced back to their original positions in the ICs. Then we computed the center of mass of these particles and the radius \( R_{\text{zoom}} \) of the smallest sphere enclosing all of them. It turns out that both these quantities are extremely stable so that the local void position, around which candidate pairs will be searched for.

5 RECOVERY OF THE LOCAL NEIGHBOURHOOD

This section deals with the issue of the stability of the main large scale structures in the nearby Universe, focusing on the properties of the Virgo cluster and the local filament. The discussion of the local void and its properties will be marginal, since its reconstruction goes beyond the scope of this paper, due to the smallness of the box size. A visual example of the reconstruction of the local neighbourhood is presented in Fig. 5, where all of the aforementioned structures can be spotted in the dark matter particles distribution and large scale velocity streams.

Naively, one could think that the presence of these objects should be granted by the very nature of the linear WF reconstruction, which is effective on these scales as shown for the CF2 data reconstruction. However, the small box and therefore the effect of periodic boundary conditions effects make the issue of correct reproduction of the local neighbourhood highly non-trivial, deserving to be treated on its own. It is only ensuring that a proper environment stems from the application of the WF/RZA/CR that one can move forward and look for LG-candidates.

In what follows, the AHF halo finder (Knollmann & Knebe 2009) has been used to find Virgo and determine its mass and position. Different algorithms can be used to define a filament (see e.g. Hahn et al. 2007; Forero-Romero et al. 2009; Sousbie 2011; Falck et al. 2012; Tempel et al. 2013; Chen et al. 2015), in this work we used the one described by Hoffman et al. (2012), which is based on the dimensionless shear tensor

\[
\Sigma_{\alpha\beta} = -\frac{1}{2H_0} \left( \frac{\partial v_\alpha}{\partial r_\beta} - \frac{\partial v_\beta}{\partial r_\alpha} \right) \tag{1}
\]

to classify a region in space given the number of positive \( \Sigma_{\alpha\beta} \) eigenvalues \( \lambda \) at that point. Namely, a void is defined as an area with no \( \lambda > 0 \), a sheet has one \( \lambda > 0 \), a filament two and a knot three. The stability of the results has been also checked computing the shear tensor over different grids (128³ and 256³ nodes) and smoothing lengths (2.5 and 3 \( h^{-1} \text{Mpc} \)), showing no particular dependence on the particular choice of their value (Libeskind et al. 2014).

In the case of the local void, we will refrain from providing a detailed quantitative analysis of our results, which is left for future studies. In fact, due to the limitations imposed by the boundary conditions, we know in advance that it is not possible to quantitatively reconstruct a structure of that size within the context of this reconstruction. It is nonetheless worth noticing that a visual inspection of density contours and velocity streamlines consistently reveals the presence of an extended underdense zone in the \( Z > 0 \) area above the center of the box. Moreover, the shear tensor eigenvalues and eigenvectors show how the push coming from this region is compatible with the observational estimates of Libeskind et al. 2015, ensuring that our local void reconstruction, albeit incom-
Table 3. Simulations settings: Number of realizations per simulation type ($N_{s\text{imu}}$), box size ($L_{\text{box}}$, in $h^{-1}$ Mpc units), radius of the Lagrangian region in the ICs ($R_{\text{zoom}}$, in $h^{-1}$ Mpc units), effective smallest mass resolution achieved ($m_p$, in $h^{-1} M_\odot$ units) and starting redshift ($z_{\text{start}}$). $m_p$ refers to the mass of the particles in the Lagrangian region of the zoom-in SimuLGzoom series; for SimuLN256 and SimuLN512 it is the mass of all DM particles since they are full box simulations with no higher resolution region.

| Name             | $N_{\text{simu}}$ | $L_{\text{box}}$ | $R_{\text{zoom}}$ | $m_p$           | $z_{\text{start}}$ |
|------------------|-------------------|------------------|-------------------|-----------------|-------------------|
| SimuLN256        | 100               | 100              | NO                | $5.26 \times 10^9$ | 60                |
| SimuLN512        | 12                | 100              | NO                | $6.57 \times 10^8$ | 80                |
| SimuLGzoom       | 300               | 100              | 12                | $6.57 \times 10^8$ | 80                |

Figure 2. Two dimensional plot of dark matter particles within a $14h^{-1}$ Mpc side slice of thickness $\pm 3h^{-1}$ Mpc, for the 100 realisations from the SimuLGzoom simulations series, showing the main structures of the local neighbourhood on the $X-Y$, $X-Z$ and $Y-Z$ planes, in supergalactic coordinates. The arrows represent the velocity field as seen in the LG frame of reference. The red circles enclose the local volume, a sphere of radius $5h^{-1}$ Mpc that represents the zone of research of LG candidates. On the $X-Y$ plane it can be seen a thin filament close to the center of the plot and connected to Virgo on the upper left corner.

5.1 Virgo

To identify the simulated Virgo candidate, one has to look for the closest and largest structure around the expected observational position in the AHF catalogs. The properties of these simulated Virgos are listed in Table 4. The first remarkable result is that the variance complete, is however satisfactory from the point of view of the Local Group and the aims of the current paper.
of the reconstructed masses and positions is small (in agreement with the findings of Sorce et al. [2016]) as can be deducted by looking at both the spread between the maximum and minimum values and the standard deviation of each of the properties shown.

This is a proof of the power of this method on these scales, even with a simulation box of only $100 h^{-1} \, \text{Mpc}$, where in principle the effect of the periodic boundary conditions could be strong enough to spoil the stability of the results. It is clear that the effect of the random modes is at best marginal and the whole reconstruction pipeline results in very stable cluster-sized Virgo look-alikes, with a median error in the reconstructed position of only $2.67 h^{-1} \, \text{Mpc}$. As a side note, it can be noticed that the $M_{200}$ is just half of the observed value for the Virgo mass, which is $> 4 \times 10^{14} h^{-1} \, \text{M}_\odot$. This is however an expected result, most likely related to the smallness of the box size. In fact, it can be shown Sorce et al. [2016] that with a box of $500 h^{-1} \, \text{Mpc}$ per side the median reconstructed Virgo mass is $\approx 3.5 \times 10^{14} h^{-1} \, \text{M}_\odot$, and is thus much closer to the observed value. Whereas this effect is known for standard $N$-body simulations Power & Knebe [2006], a detailed investigation of the correlation between the box size and mass of the local supercluster in CSs is beyond the scope of this work and is left for a separate analysis. For the aim of this paper it is sufficient to prove that our local neighbourhood reconstruction includes a cluster-sized object, placed at the right position, whose properties are largely independent from the specific random realisation. A stable Virgo look-alike is hence the first result of the WF/RZA/CR pipeline, in agreement with the findings of Sorce et al. [2016] and a substantial improvement over the past outcomes of constrained simulations performed with observational data Gotloeber et al. [2010], where reconstructed local superclusters had a position displacement $> 10 h^{-1} \, \text{Mpc}$ with respect to the expected value.

5.2 The Local Filament

Filaments are identified using the same procedure described in Section 5 based on the algorithm of Hoffman et al. [2012]. It is important to remark that the use of a smoothing length of $2.5 h^{-1} \, \text{Mpc}$ is dictated by the need to compare to observations, filtering out nonlinearities induced by the unconstrained short wave modes.

The local filament can be found by looking at structures around the center of the box. Since the reconstructed Virgo position turns out to be displaced by $\approx 2.5 h^{-1} \, \text{Mpc}$ with respect to the observational value, one would first look for the local filament at a position shifted by an equal amount from the box center. However, it turns out that nearest grid point (NGP) of such a displaced position would have (in almost all realisations) only one positive eigenvalue, meaning that the environment should be classified as a sheet. Indeed, the center of the box is an excellent choice to look for a filament, since in 87 out of 100 cases the NGP is characterized by two positive eigenvalues. Moreover, even in the remaining 13 cases a filament can be always found within $\approx 5 h^{-1} \, \text{Mpc}$ from the center, meaning that this kind of structure is a constant feature of the expected LG position.

To quantify the goodness of our filament reconstruction we compare our results to Libeskind et al. [2015], which were previously shown in Table 1. In Fig. 3 are plotted the $\lambda$s and their standard deviations, noticing that our estimated values are in very good agreement with their findings. This means that the strength of matter accretion along $e_1$ and $e_2$ and expulsion along $e_3$ is very well reproduced by the simulated filament. Moreover, not only the intensity but also the directions of the eigenvectors are well reproduced, as shown in Table 5. In fact, the small values of $\sin \theta$ presented there (defining $\theta$ as the angle between reconstructed $e_i$ and $e_3^{WF}$) indicate a good alignment between the two vectors.

6 RECOVERY OF THE LOCAL GROUP

Once it is ensured that the reconstruction methods employed here give rise to a configuration of the local neighbourhood which is both stable and realistic, one can start to look for possible LG candidates. As we discussed in Section 4 resolution-related problems were bypassed designing a series of zoom-in simulations (labeled SimuL5zoom) with a sufficient number of smaller mass particles just around the expected LG position. The white noise field of these simulations has been generated in the following way. We selected 40 white noise fields from different SimuL5 runs, to have a sufficient number of different CR of the large scales to factor out possible specific seed-related effects. Then, for each of these fields were generated five to ten different random realisations of the additional layer of refinement in the Lagrangian region, using Ginnungagap giving rise to different sub-Mpc configurations. For some of these realisations, it has been checked that the results in the zoom-in regions overlap with those taken from the set of SimuL512 full box $512^3$ simulations.
Table 5. Comparison between CF2 values for the eigenvectors and eigenvalues at the LG position (taken from Libeskind et al. (2015)) and simulations. Table (a): Averages and standard deviations for the sines of the angles of alignment between simulated and observational eigenvectors. Table (b): Mean values and standard deviations for the eigenvalues at the LG position.

|      | simu   | obs    |
|------|--------|--------|
| sin θ_1 | 0.174 ± 0.062 | 0.148 ± 0.038 |
| sin θ_2 | 0.052 ± 0.075  | 0.051 ± 0.039  |
| sin θ_3 | −0.270 ± 0.074 | −0.160 ± 0.033 |

(a) (b)

Figure 4. Particle densities in a 5h⁻¹ Mpc side slice of thickness ±2h⁻¹ Mpc showing the candidates M31 and MW in a single realisation, along the X − Y, X − Z and Y − Z planes.

6.1 Identification criteria

The first issue that is encountered in the identification of the LG candidates is related to the details of the definition of a LG-like object. Indeed, given both the observational uncertainties and uneven relevance of the many LG-defining properties to some general problems, the debate on what really constitutes a meaningful candidate is far from settled and several authors in the past have used different criteria (e.g. Forero-Romero et al. 2013; González et al. 2014; Sawala et al. 2014; Libeskind et al. 2015) to define LG-like pairs in cosmological simulations. Due to the predominance of the random component at sub-Mpc scales, it is not expected that these objects should be a feature of the simulations in the same way the local neighbourhood was, so that imposing restrictive identification criteria from the very start might conceal other interesting results. Moreover, there is a huge number of variables that could
be checked and used as criteria to match a simulated LG to the real one. Therefore, we decided to split the identification issue into several steps, taking into account an increasingly larger subset of variables to define our candidates. Namely, we introduced (1) a first broad selection criterion based solely on the mass and position of isolated halo pairs, (2) a second one based on the requirement that angular momentum and energy fall within observational bounds and (3) additionally restricting our sample to pairs with radial and tangential velocities compatible to the LG values. In what follows, we will refer to LG-gen as the first LG-compatibility criterion, LG-dyn as the second one and LG-vel as the third one.

Specifically, a LG-gen-type LG candidate will satisfy the following requirements:

- the total mass of the halo pair must be smaller than $5 \times 10^{12} h^{-1} M_{\odot}$
- the mass of the smallest candidate must be larger than $5 \times 10^{11} h^{-1} M_{\odot}$
- the distance $d$ between the two haloes must satisfy $0.3 < d < 1.5 h^{-1} \text{Mpc}$
- there is no other halo of mass greater or equal than the smallest candidate within a radius of $2.5 h^{-1} \text{Mpc}$
- the center of mass of the halo pair must be located within $5 h^{-1} \text{Mpc}$ from the box center

This criterion allows us to obtain a first assessment of the success of our method in producing isolated halo pairs at the right position and with a mass of roughly a factor two within the observational constraints on the LG (similar criteria were used by Forero-Romero et al. [2013] Libeskind et al. [2015]). These are general prerequisite characteristics of any realistic LG, and allow us to construct a first large halo sample which could be used to address a general prerequisite characteristics of any realistic LG, and allow us to construct a first large halo sample which could be used to address a large number of open issues, such as the use of the timing argument.

To identify LG-dyn halo pairs the approach of Forero-Romero et al. [2013] was followed, considering the (reduced) values of energy angular momentum of the LG-gen candidates to identify those whose global dynamic status is compatible with the actual observations. Defining

$$e = \frac{1}{2} v_{51}^2 - \frac{G M}{r_{51}}$$ (2)

as the reduced energy and

$$l = |r_{51} \times v_{51}|$$ (3)

as the reduced angular momentum, one can proceed generating contours in the $e - l$ plane through 10$^7$ Monte Carlo iterations, realised drawing from the observational values listed in Table 2 and assuming Gaussian priors on the 2$\sigma$ intervals. Then, for each LG-gen pair $e$ and $l$ are computed and all those pairs that fall within the 95% contours are labeled as LG-dyn-type. LG-vel candidates are those whose radial and tangential velocities fall within 2$\sigma$ of the observational values.

### 6.2 Local Group like objects

Using the identification criteria outlined in the previous section, one starts looking for potential LG candidates in each of the 300 SimuLN256 realisations. We proceed as follows. First, a sphere of $5 h^{-1} \text{Mpc}$ is taken around the box center and all the LG-gen halo pairs therein are listed. The environmental type is then determined associating each halo to its NGP on a 256$^3$ grid, where the eigenvalues of the shear tensor were previously computed. In this way we can double-check the results of Section [2] and make sure that one can identify a filament also at the actual LG position. Finally, one can look at the dynamics of the LG-gen candidates. On the one hand, it is interesting to see whether their conserved properties are generally compatible with the observed ones in the sense of the LG-dyn criterion, singling out candidate pairs disregarding the specific transient dynamical state. On the other hand, however, one can also be interested in checking whether some of those pairs actually have radial and tangential velocities in agreement with observations (type LG-vel). Table 6 shows the number of candidates according to each selection criterion.

The first important thing to notice is that in approximately half of the simulations (146 out of 300) it is possible to identify a LG-gen-type of candidate within $5 h^{-1} \text{Mpc}$ of the expected position. These objects are then characterised by the NGP eigenvalues of the two haloes, allowing the pair to be composed of objects living in different environment types. Checking the numbers explicitly for each candidate pair, we find that 120 out of 146 candidates actually belong to a filament. This is an important result for the CSs: one can produce at a 40% rate objects that can be broadly classified as LGs, within just $5 h^{-1} \text{Mpc}$ from the expected position and that live within a filament. Fig. 6 offers a visual impression of one of such LG candidates for a single realisation, where the two main haloes can be clearly seen within a filamentary stream of dark matter particles. It is quite clear that such a high success rate has to bear a connection to the shown stability of the local neighbourhood. However, such an investigation is beyond the scope of the present paper and will be dealt with in a following work.

One can compare these rates to what has been found by other authors in the literature to quantify the improvement obtained over previous results. For instance, Fattahi et al. [2015] found 12 objects looking within a random cosmological simulation box of $100 h^{-1} \text{Mpc}$ per side, corresponding to a density of $1.2 \times 10^{-4} h^{-1} \text{Mpc}^3$. Their selection criteria are based on:

- relative radial velocity between $-250$ and $0 \text{ km s}^{-1}$
- relative tangential velocity smaller than 100
- separation between 600 and 1000 kpc
- total pair mass in the range $\log(M_{\text{tot}}/M_{\odot})$

Applying these very same constraints on our CSs, a total of 75 objects can be identified. Since our search volume is made up of 300 spheres of radius $5 h^{-1} \text{Mpc}$, the density of LG-like pairs is $4.77 \times 10^{-4} h^{-1} \text{Mpc}^3$, that is a factor of 40 larger. Beside the higher production rate, it has to be stressed that each pair is placed within a large scale environment that closely matches the observed one, which is the most relevant feature of the CS method.

To analyze the dynamical properties of this LG-gen halo sample, the focus is placed on $e$ and $l$, the reduced energy of the system and its reduced angular momentum. Ideally, in a completely iso-

| Type   | N   | $N_f$ |
|--------|-----|------|
| LG-gen | 146 | 120  |
| LG-dyn | 51  | 42   |
| LG-vel | 6   | 6    |
related system, these two quantities would be conserved. However, due to the non-ideal nature of the LG this is only partially true. Because of the high degree of isolation implied by our definition of the LG, the expected departure from the ideal case is small. Consequently, it is expected that $e$ and $f$ are almost perfectly conserved, allowing for a more robust classification of the pair. In fact, it could be misleading to look at distances and velocities only, since these quantities are transient by their very nature and might not reveal the fundamental properties of the pair, which might have looked (or will look) much closer to today’s LG values at some other moment in time. By looking at semi conserved quantities, instead, one is able to single out those structures which have most likely formed with the same local initial conditions and compare their histories and evolution. Indeed, the reconstruction in a statistical sense of the history and evolution of the LG is one of the ultimate goals of the CLUES collaboration. As described in the previous paragraph, LG-dyn candidates were identified as those halo pairs falling within the Monte Carlo generated 95% confidence intervals in the $e - l$ plane, selected from the previously identified LG-gen-type objects located on a filament. These candidates are plotted in Fig. 5. From there and from Table 6, one sees that the number of such object is non-negligible, as one can find 42 pairs, corresponding to a 14% success rate. Again, this is a striking result, since it shows that CSs can produce at a significant pace isolated halo pairs whose global dynamical state is compatible with the observations for the LG. Moreover, these pairs are selected among the larger LG-gen sample, which was already constraining their mass and separation, ensuring that none of these LG-dyn candidates has properties too far off from realistic values. In fact, it could in principle be possible to produce LG-dyn-only pairs with unrealistic values of mass and velocities that could nonetheless conspire and give rise to a compatible $e - l$ combination. It has to be noticed that most of the LG-gen-candidates lying outside of the 95% confidence intervals are located towards the upper right corner of the $e - l$ plane, meaning that potential pairs tend to have high angular momenta as well as low binding energies.

As a final test, one can further narrow down the sample to look for LG-vel-pairs, with $v_{\text{rad}}$ and $v_{\text{tan}}$ within $2\sigma$ from the observational values, resulting in a total sample of 6, a factor of ten smaller compared to the total number of LG-dyn-type objects embedded in a filament. This lower number is hardly surprising given the fact

Figure 5. LG-gen isolated halo pairs. Solid lines show the dynamical states compatible with LG observations, determined by $10^7$ Monte Carlo random realisations. Each halo pair that falls within the 95% confidence intervals belongs to the LG-dyn sample.

| Table 7. Properties of the LG candidates with observationally compatible radial and tangential velocities. $M_{MW}$ and $M_{M31}$ are expressed in $10^{12} h^{-1} M_\odot$ units and refer to the smaller and larger haloes of the pair. $R$ is the distance between the two halo centers (in $h^{-1}$ Mpc) whereas the tangential and radial velocities are expressed in km s$^{-1}$. |
| --- | --- | --- | --- | --- |
| $M_{M31}$ | $M_{MW}$ | $R$ | $V_{\text{rad}}$ | $V_{\text{tan}}$ |
| 1.54 | 0.59 | 1.45 | -101.2 | 6.6 |
| 3.08 | 1.11 | 1.01 | -116.4 | 16.5 |
| 2.49 | 1.19 | 1.32 | -99.5 | 32.3 |
| 2.08 | 0.61 | 1.48 | -119.5 | 11.3 |
| 2.80 | 0.97 | 1.03 | -117.1 | 35.1 |
| 1.01 | 0.73 | 0.59 | -102.7 | 10.3 |

that these quantities are transients and are thus even more subject to the randomness of the short wave modes. Nonetheless, it is possible to produce a few candidates with the right tangential and radial velocities at $z = 0$, which could be the starting point for future high resolution zoom in simulations.

### 6.3 Shear tensor analysis

Having identified a large number of LG candidates one can extend the analysis of the shear tensor eigenvalues and eigenvectors at its position, along the lines of what was done in Section 5 at the center of the box, i.e. the expected LG position. To do this, each halo belonging to the candidate LG is assigned to the NGP, computing the mean and standard deviation of the three $\lambda$s, to properly account for those pairs whose members belong to different nodes on the cosmic web. Indeed, as shown in the previous section, only 26 out of 146 LG-gen candidates were living on different kinds of environment, whereas the remaining 120 pairs both belonged to a filament, though some of them characterized by different sets of eigenvalues and eigenvectors. Moving to the eigenvector basis in each simulation, we then look for correlations to the large scale environment computing the cosines between $e_1$, $e_2$, $e_3$ and $e_{\text{Virgo}}$, the direction of Virgo from the center of mass of the LG, showing the alignment of the latter to $e_3$.

| $e_1$ | $e_2$ | $e_3$ |
| --- | --- | --- |
| $e_{\text{Virgo}}$ | 0.28 $\pm$ 0.24 | 0.30 $\pm$ 0.21 | 0.92 $\pm$ 0.10 |

To summarize, we have shown that we can use CSs as a Local Group Factory: A numerical pipeline for producing isolated halo pairs, living on a filament stretched by a large cluster and pushed by a large nearby void, whose properties can be shown to be broadly compatible with observational data of the real LG.
7 CONCLUSIONS

We have demonstrated here how the combined Cosmicflows-2 data, the ΛCDM model and the WF/RZA/CR methodology effectively give rise to Local Group-like objects, in an environment which closely mimics the actual local neighbourhood, in constrained cosmological simulations. The main improvements, in the methodology and the observational data, introduced since the first generation of the CLUES simulations (Yepes et al. 2014) have been reviewed. We rely heavily on our recent Sorce et al. (2016) paper and extend it to focus on the simulation of the LG and its close neighbour. We have shown how the data, cosmological model and the methodology conspire together to yield a robust ‘factory’ that produces simulated LG-like objects in abundance.

The simulations reported here are all DM-only and are done within a 100h⁻¹ Mpc box. The ΛCDM model is assumed with the Planck set of cosmological parameters. Three sets of simulations have been performed: SimuLN256: designed to study the stability of the large scales with respect to the constrained variance; SimuLN512: in which the effect of the mass resolution is studied; and SimuLZoom: where zoom-in techniques is used to produce high resolution LGs and are used to study statistically the simulated LGs.

Our main findings fall into two classes. One concerns the environment of the LG and the other deals with the properties of the two halos that constitute the simulated LGs. It should be emphasized here that essentially all the LGs are embedded in an environment which closely resembles the actual one. A summary of these findings follows:

1. The local environment, represented here by the Virgo cluster and the local filament are a robust outcome of the CF2 data and the ΛCDM model. Quantitative analysis yields:
   1a. The mean offset in the position of the simulated Virgo’s (from the observed one) is a mere 2.67h⁻¹ Mpc. The median and scatter of the mass of the simulated Virgo is 2.09 ± 0.69 × 10¹⁴h⁻¹M⊙. This is roughly smaller by a factor 2 from common estimates of the Virgo mass. The smallness of the present computational box accounts for a factor of ≈2 suppression in the mass of the simulated Virgo (cf. Sorce et al. 2016).
   1b. The cosmic web is defined here by the V-web, which is based on the analysis of the velocity shear tensor. The simulated local environments recover the directions of the eigenvectors and magnitude of the eigenvalues. Roughly 90% of the simulations recover the local filament at its expected position and 80% of the identified LGs reside in a filament similar to the observed local filament. The 100h⁻¹ Mpc computational box is too small to reproduce the Local Void, but the analysis of the simulated velocity shear tensor recovers its repulsive ‘push’ at the position of the LG.

2. The frequency, or success rate of the production of simulated LGs: Two sets of criteria have been used to identify LG-like objects. The first consists of the masses of the two main halos, their distance and isolation. The other set adds to the first one also kinematic constraints on semi-conserved quantities, namely the energy and orbital angular momentum. The first set of criteria (LG-gen) yields isolated halo pairs, neglecting their particular dynamic state, while the second one (LG-dyn) singles out candidates whose energy and angular momentum are compatible with observations. We have further refined these criteria to objects with the right phase on their orbit, defined by their energy and angular momentum, so as to capture the observed radial and tangential velocities (LG-vel). These sets of criteria yield:
   2a. Out of a total of 300 SimuLZoom runs, a total of 146 LG-gen-type objects were identified.
   2b. The fraction of LGs goes down to 17%-51 out of 300, when adding energy and orbital angular momentum constraints. Out of these 51 LG-dyn candidates only 6 are on the same phase on the orbit as the actual LG - these are within 2σ of the observed radial and tangential velocities.

The LG factory provides a robust tool for producing ensembles of LG-like objects and their environments. The effort of obtaining an ensemble of 100, say, LGs, depends on the definition of a LG. Roughly 200 constrained simulations (of different realizations of the ICs) are needed to reproduce 100 LGs defined by their isolation, mass and separation distance. Adding the orbital (energy and angular momentum) constraints the number of required simulations rises to 500. Adding the phase constraint, namely of the radial and tangential relative velocities, 2700 simulations must be performed to obtain an ensemble of 100 LGs with the required properties.

An inherent tension exists between the fields of cosmology and the near field cosmology and between the use of random and constrained (local universe) simulations. It relates to the Copernican question of how typical is the LG, and thereby to what extent the LG and the local neighbourhood constitute a typical realization of the universe at large. The answer to this question will determine whether the terms ‘near field’ and ‘cosmology’ can be paired together. The LG factory provides a platform for systematic and statistical studies of the problem and thereby sheds light on the relevance of the near field to cosmology at large. One qualitative results can already be drawn from the present study. Our results show that the LG is a likely outcome of the CF2 data and the assumed ΛCDM model.

The present paper serves as a proof of concept for our method. It also opens the road to a wide range of applications. It enables the construction of a very large ensemble of constrained simulations which harbour realistic LG-like objects and their environment. Such an ensemble can be used to study the (constrained) nature of the LG. Suitable members of the ensemble can be selected as suitable ICs for simulations. Such simulations can include both DM-only and full hydro high resolution simulations. We intend to pursue these and other applications of our method.

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