INTRODUCTION

It is well accepted that plant species and their interactions affect grassland biomass yields (Hector, Bell, Connolly, Finn, & Fox, 2009). Biodiversity-Ecosystem Function (BEF) analyses aim to quantify these effects and determine to what extent specific species combinations affect yield responses (reviewed in Cardinale et al., 2007; Hector et al., 2009). While simple in concept, this task is mathematically challenging and complicated by increasing interspecific variation (Connolly et al., 2013; Fibich, Rychtecká, & Lepš, 2015).

One approach used to assess diversity effects is Diversity-Interactions (DI) modeling (Kirwan et al., 2007, 2009).
Diversity-Interaction models quantify species identity effects and diversity effects using a regression framework that combines weighted species monoculture performances with interaction terms to find expected mixture responses (Kirwan et al., 2007, 2009). A general expression of a DI model is:

$$y = \text{ID} + \text{DE} + \varepsilon$$ (1)

where $y$ is the ecosystem function, ID stands for “identity effect” and can be extended to include treatment or block effects, DE stands for “diversity effect”, and $\varepsilon$ is the error term, typically assumed independent and identically distributed $N(0,\sigma^2)$.

Derivations of this model include a series of progressively complex DE terms used to characterize alternative species interaction scenarios. The simplest model assumes that species do not interact with one another and that mixture yields are proportional to species monoculture yields (M1: identity model). Additional models allow all species to interact equally, regardless of their species or functional identity (M2: average pairwise model), for each species to contribute uniquely to pairwise interactions regardless of the identity of the other species (M3: additive species-specific model), and for species to interact differently within and between functional groups (M4: functional group model; details in Methods section). Once these models are fit, model comparison tests are used to determine which interaction scenario best describes observed ecosystem functions.

Diversity-Interaction models can also test for effects of additional experimental treatments on diversity responses by adding ID and DE interaction terms (Kirwan et al., 2009). This is useful when considering to what extent plant species fine-scale spatial relationships affect plot-scale diversity effects. Plant species interact on finite-scales, and if their interaction distances are small enough, their spatial relationships can presumably affect the interactions they experience and respond to (Houseman, 2014; Lamošová, Doležal, Lanta, & Lepš, 2010; Murrell, 2010; Porensky, Porensky, Vaughn, & Young, 2012; Seahra, Yurkonis, & Newman, 2019; Stoll & Prati, 2001; Yurkonis & McKenna, 2014). In spatially manipulated tallgrass prairies, increasing species interspecific interactions increased biomass and favored clonal forbs (McKenna & Yurkonis, 2016), an effect that was replicated by seeding species in smaller conspecific patches (Seahra, Yurkonis, & Newman, 2019). However, manipulating species pattern had a neutral effect on plot-scale species interactions (quantified by the Additive Partitioning method; Loreau & Hector, 2001) in these studies (McKenna & Yurkonis, 2016; Seahra et al., 2016). In both cases, species responses to changes in their interaction neighborhoods were likely so species specific that positive and negative pattern effects combined to create a neutral overall diversity effect. Because DI models can expressly quantify species contributions to DE in response to treatments, they provide an avenue to more specifically elucidate how species interaction neighborhoods affect tallgrass prairie diversity.

As with other BEF modeling approaches, DI models require users to a priori determine how each species is expected to proportionally contribute to community effects. Expected species proportions can be set based on the number of individuals (e.g., sown or planted individual proportions) or on the relative size (proportional biomass) of each species in mixture. If species interactions are proportional to their size, setting species proportions based on their relative biomass (e.g., by replacing individual based proportions with first or subsequent year proportional biomass) may improve BEF model fit (Finn et al., 2013; Grace, Keough, & Gutenspergen, 1992; Kirwan et al., 2009). However, this would be ineffective if the outcome of species interactions were unrelated to their aboveground biomass. This could occur if wide swings in species-specific biomass production occur from year to year to affect the rank-order of species among growing seasons (Brophy, Finn, et al., 2017; Finn et al., 2013). In this case, diversity effects may be best explained by simply setting species proportions based on their relative number of individuals. While Finn et al. (2013) found that adjusting for species previous year proportional biomass improved DI model fit, using the “planted proportions of individuals” approach may provide a better model fit for communities with large or variable species pools.

In this study, we tested effects of species interactions on plant biomass production by applying DI models to the first three years of biomass data collected from a grassland biodiversity experiment. We address the following questions:

1. Which diversity effect framework (M1–M4) best describes plot biomass?
2. Are diversity effects affected by species planting pattern?
3. Are interactions that affect plot biomass better described based on species individual (planted) proportions or their previous proportional biomass?

2 | METHODS

2.1 | Experimental design

The Species Pattern and Community Ecology (SPaCE) experiment (North Dakota, USA) consists of 1 m × 1 m field plots planted with greenhouse grown seedlings in June 2012. The field had been in row crop production for the previous 15 years and was planted with spring wheat in the previous growing season. Plots varied in species richness (2, 4, 8 species and monocultures), evenness (low, intermediate, high), and pattern (dispersed and aggregated). Plots were spaced 2 m apart with mown aisles and arranged in a randomized complete block design with five blocks. At planting, we divided each plot into an 8 × 8 grid of 64 planting cells and planted a single seedling in each cell. For the pattern treatment, we either randomly assigned individuals to each of the 64 planting cells (“dispersed” treatment) or we randomly assigned individuals of each species to a 2 × 2 set of four cells (“aggregated” treatment). With this design, we increased conspecific interactions among nearest neighbors in aggregated plots relative to dispersed plots. For the evenness treatment, we altered the number of individuals planted from each species within each richness level. In two-species plots, the ratio of individuals of each species was either 8:56 (low), 16:48 (intermediate), or 32:32 (high). In four species plots, the ratio of individuals was either 4:4:28:28, 8:8:24:24, or 16:16:16:16. In eight species plots, the
ratio of individuals was either 4:4:4:4:8:16:20, 4:4:4:4:12:12:12, or 8:8:8:8:8:8:8. Species were selected from a pool of 16 common tallgrass prairie species (Table 1) and randomly assigned to plots with the following functional group constraints: two-species plots contained a grass (warm or cool season) and a legume or a forb, four species plots contained one species from each functional group, and eight species plots contained two species from each functional group. We additionally randomly assigned species to abundance levels within each plot, which resulted in some variation across species in their average planted proportions across all treatments (range 16%-28%; Figure 1a).

We weeded the plots monthly during the growing season to remove volunteers from the local propagule pool and any nonassigned species from the study species pool. At the end of each of the three growing seasons (September 2012, 2013, and 2014), aboveground biomass was cut to 5 cm above the soil surface, sorted to species,
dried to a constant mass (60°C), and weighed. Further experimental
details are provided in McKenna and Yurkonis (2016).

We used total and species-specific aboveground biomass data
from 170 plots of the SPaCE experiment for this analysis (3 levels rich‐
ness × 3 levels evenness × 2 levels species spatial pattern = 18 mix‐
tures + 16 monocultures = 34 plots × 5 blocks = 170 plots). For
each plot, we calculated the planted proportion of each species (planted
proportion = # individuals for species i/64 subplots) and the propor‐
tional biomass of each species in each year (realized proportion = har‐
est biomass of species i/total plot biomass; Figure 1b–d). We used
species planted proportions as predictors in our Diversity‐Interactions
(DI) modeling analysis of year 1 total plot biomass. We used species
planted proportions and separately used species realized proportions
in our DI modeling analysis of year 2 and year 3 total plot biomass.

2.2 | Application of Diversity‐Interactions (DI)
models to SPaCE data

We considered a series of four hierarchical DI models to describe
yearly plot biomass and test alternative hypotheses about species
interactions in the plots. These models were related to a realization
of Equation (1), the “full pairwise interaction” model wherein.

\[
y = \sum_{i=1}^{S} \beta_i P_i + a_b + \sum_{i \neq j}^{S} \delta_{ij} P_i P_j + \epsilon
\]  

where \(y\) is total plot biomass, \(S = 16\) is the total number of species in
the pool (Table 1), \(P_i\) is the reference proportion of species \(i\) (either
planted or realized in the preceding year), \(\beta_i\) is the expected mono‐
culture yield of species \(i\), \(a_b\) is the effect of block \(b\), where \(b = 1,...,5\), \(\delta_{ij}\)
is the potential for two species to interact, \(\delta_{ij} P_i P_j\) is the contribu‐
tion to biomass resulting from the interaction of species \(i\) and \(j\) and \(\epsilon\)
is assumed i.i.d. \(N(0,\sigma^2)\). Since there are a large number of possible
pairwise interactions for this 16‐species system
\[\binom{120}{16} = \binom{16}{2}\text{, we considered four DI models that imposed some constraints among the }\delta_{ij}\text{ (DE) coefficients (Kirwan et al., 2009).}

Model 1 (M1): The “identity” model assumed that species do not in‐
teract with one another, that is, \(\delta_{ij} = 0\) for all \(i, j\). In monoculture,
the expected performance of species \(i\) is \(\beta_i\), adjusted for block. In
mixture, the expected plot yield is a weighted average of the spe‐
cies expected monoculture performances, adjusted for block, and
it is assumed that there are no interaction effects. The equation is:

\[
y = \sum_{i=1}^{S} \beta_i P_i + a_b + \epsilon \quad \text{(M1)}
\]

Model 2 (M2): The “average pairwise interaction” model assumed
all pairs of species interacted with one another in equal strength,
that is, \(\delta_{ij} = \delta\) for all \(i, j\). The equation is:

\[
y = \sum_{i=1}^{S} \beta_i P_i + a_b + \delta \sum_{i \neq j}^{S} P_i P_j + \epsilon
\]

Model 3 (M3): The “additive species‐specific interactions” model
assumed that each species contributed a unique and constant
(additive) coefficient to its interaction with every other species,
regardless of the identity of the other species in the interaction.
The expected interaction for any pair of species is the sum of
their two unique coefficients, that is, \(\delta_{ij} = \lambda_i + \lambda_j\) for all \(i, j\). The equation is:

\[
y = \sum_{i=1}^{S} \beta_i P_i + a_b + \sum_{i \neq j}^{S} (\lambda_i + \lambda_j) P_i P_j + \epsilon
\]

Model 4 (M4): The “functional group” model assumed that pairs of
species from the same functional group \(k = 1,...,4\); cool‐season
grass, warm‐season grass, forb, and legume; Table 1) interacted in
the same way, that is \(\delta_{ij} = \omega_k\) for all \(i \neq j\) from the \(k\)th functional
group, and that pairs of species from different functional groups
\(k\) and \(l\) interacted in the same way, that is \(\delta_{ij} = \omega_k\) for all \(i\) from
the \(k\)th functional group and all \(j\) from the \(l\)th functional group. Thus,
the functional group model included ten interaction parameters,
with “within functional group” interactions: \(\omega_{11} , \omega_{12} , \omega_{13} , \omega_{14} , \omega_{22} , \omega_{23} , \omega_{24} , \omega_{33}, \omega_{34}, \omega_{44}\). The equation is:

\[
y = \sum_{i=1}^{S} \beta_i P_i + a_b + \sum_{k=1}^{T} \omega_k \sum_{i \neq j}^{T} P_i P_j + \sum_{i \neq j}^{T} \omega_{k} \sum_{i \in FG_k,j \in FG_l}^{S} P_i P_j + \epsilon
\]

\[\text{where } T = 4 \text{ and } FG_1 = \{1,2,3,4\}, FG_2 = \{5,6,7,8\}, FG_3 = \{9,10,11,12\},
FG_4 = \{13,14,15,16\} \text{ and the species names are given in Table 1.}
Models (M1–M4) inherently account for the SPaCE experiment
richness and evenness treatments by including the species pres‐
ent and their expected plot‐scale proportions when predicting
plot biomass yields. To account for the species pattern treatment,
we expanded these models to test for interactions of the pattern
treatment with DE terms in mixture plots. For example, the ex‐
panded version of model 2 (M2) is:

\[
y = \sum_{i=1}^{S} \beta_i P_i + a_b + \delta \sum_{i \neq j}^{S} P_i P_j + \epsilon
\]

\[
\times Sp + \epsilon
\]
where spatial pattern (Sp) is coded 1 for aggregated plots, 0 for dispersed plots, and 0 for monocultures. The term $\delta_2$ is the interaction between any pair of species in dispersed plots. The term $\delta_3$ allows for a change in the interaction between any pair of species in aggregated plots.

We expanded the model further to test for interactions of the tall-statured, rhizomatous forb, *Helianthus maximiliani* (HM, Maximilian sunflower, species # 11 in Table 1) with the DE terms. For example, the expanded version of Equation (3) is:

$$y = \sum_{i,j=1}^{S} \beta P_i + \alpha_1 \delta_1 P_j + \delta_2 \sum_{i,j=1}^{S} P_i P_j \times Sp + \delta_3 \sum_{i,j=1}^{S} P_i P_j \times P_{11} + \epsilon$$

The term $\delta_3$ in Equation (4) allows for a change in the species pairwise interactions between mixtures with and without *H. maximiliani* by scaling $\delta_3$ by its reference (planted or realized) proportion ($P_{11}$; $P_{11} = 0$ for mixtures without species 11). This statistical three-factor interaction allows for a nonsymmetric species interaction effect as the proportion of *H. maximiliani* changes. We treated *H. maximiliani* separately because of lack-of-fit in models that did not include these additional interactions. Specifically, we identified patterns in residuals related to the proportion of *H. maximiliani*. This was not surprising, since *H. maximiliani* was considerably more productive than the other species in monoculture and *H. maximiliani* mixtures were more productive and more variable than non-*H. maximiliani* mixtures (Figure 2).

We fitted Models (M1–M4) separately for each year following a hierarchical process (details in Appendix S1). We used species planted proportions as the predictors for year 1 and separately used species planted proportions and realized proportions as predictors for years 2 and 3. Raw data visualizations (Figure 2) and initial model diagnostic tests showed that the error variances were not constant for all models. More flexible error structures that allowed the variance to change depending on plot characteristics (such as whether or not the plot was a monoculture, or whether or not *H. maximiliani* was included in a mixture) were tested and used where required (Brophy, Dooley, et al., 2017; Connolly et al., 2018; details in Appendix S1). We used F-tests or likelihood ratio tests (as appropriate) for model comparisons throughout the model fitting process (details in Appendix S1). After we identified the best fixed effects model, we determined if any additional variation could be accounted for by including all pairwise interactions as random effects, each constrained to have the same variance (Brophy, Dooley, et al., 2017). If random effects were needed in the model, this approach accounted for the remaining uncertainty in a parsimonious way. We carried out all analyses in SAS version 9.3 or SAS University Edition (SAS Institute Inc., Cary, NC, USA).

![FIGURE 2](image)

**FIGURE 2** Box plots of species monoculture ($n = 5$) and mixture yields over the first three years of the SPaCE experiment. Mixtures were separated by those with and without *Helianthus maximiliani* (HM). Species are ordered by their average monoculture yields in year 1. Means are indicated by dashed lines.

### 3 | RESULTS

#### 3.1 | Year 1

In the first growing season, M2, the average pairwise model, modified so that the DE term interacted with the planted proportion of *H. maximiliani* was the best model (Table 2; full model specification in Appendix S1). With this model, the diversity effect increased as *H. maximiliani* increased. For example, the estimated DE for a 4-species community without *H. maximiliani* and with 25% of each species was $35.1 \pm 15.82$. This increased sevenfold in the presence of *H. maximiliani* such that when one of the four species was *H. maximiliani*, the estimated DE was $255.19 \pm 59.9$. This positive DE means that there is a positive benefit to mixing species beyond what they contribute to plot biomass based on their monoculture performance. In this case, diversity effects were not determined by the species present, their functional identity, or their spatial pattern beyond the effects of *H. maximiliani*.

#### 3.2 | Year 2

By the end of the second growing season, the identity of the species present and their spatial pattern affected plot biomass. In year 2, M3, the additive species-specific model, based on species planted proportions and with DE terms interacting with both the proportion of *H. maximiliani* and the spatial pattern treatment was the best model (Table 2, Appendix S1). This model assumed that
TABLE 2 Summary of the best-fit models in each of the three years of the SPaCE experiment. Model selection followed a hierarchical process (outlined in methods, Appendix S1, and in Table S1.1). We tested the best model under each year-proportion scenario for additional interactions between the diversity effect terms (DE) and the study species spatial pattern treatment (Sp) and the proportion of Helianthus maximiliani (P11). Best-fit planted and realized models were compared with AIC in years two and three. Conditions of the final best model in each year are indicated in bold text. The number of fixed parameters is shown for each model as: # identity (ID) terms + # block terms + # diversity effect (DE) terms.

| Year | Proportion | Best model       | Additional interactions                        | No. Parameters | ΔAIC |
|------|------------|------------------|-----------------------------------------------|----------------|------|
| 1    | Planted    | M2: Average pairwise | (DE) * P11                                  | 16 + 4 + 2     |      |
| 2    | Planted    | M3: Additive species | (DE) * P11 + (DE) * Sp                        | 16 + 4 + 48    | 16.5 |
|      | Realized   | M3: Additive species | (DE) * P11 + (DE) * Sp                        | 16 + 4 + 48    |      |
| 3    | Planted    | M3: Additive species | (DE) * P11 + (DE) * Sp + Random Pairwise      | 16 + 4 + 48    |      |
|      | Realized   | M2: Average pairwise | -                                             | 16 + 4 + 1     | 16.5 |

Each species contributed a unique and constant coefficient to its interaction with every other species and that this species-specific contribution changed in the presence of H. maximiliani and with the spatial pattern treatment. We found no evidence of species-specific contributions to biomass being related to their functional identities.

We used heat maps to visualize predicted total plot biomass from the best-fit model fitted to the full dataset and without any out of sample verification (Figure 3). For simplicity, we show total predicted biomass (ID and DE combined) for two-species (50:50) plots and three-species plots with 20% H. maximiliani (40:40:20). Two-species (50:50) plots were predicted to be most productive when containing the larger statured species, H. maximiliani, Solidago rigida, and Astragalus Canadensis (Figure 3a). Andropogon gerardii and S. rigida were predicted to benefit the most when planted in an aggregated species pattern compared with the dispersed species pattern. In contrast, Sorghastrum nutans was predicted to suffer the most under the aggregated species pattern treatment (Figure 3a vs. 3b). When 20% of H. maximiliani was introduced into any two-species mixture, there was an automatic predicted benefit since H. maximiliani was one of the highest yielding species in year 2. This effect was picked up via the ID effect in the best-fit DI model and can be seen by the generally "redder" coloring of Figure 3a versus 3c. Including an additional 20% of H. maximiliani was also predicted to improve the ability of A. gerardii, Ratibida columnifera and Elymus Canadensis to interact with other species and reduce the ability of Desmodium canadense to interact with other species (Figure 3a vs. 3c).

3.3 | Year 3

By the end of the third growing season, the identity of the species present and their spatial pattern continued to affect plot biomass. In year 3, M3, the additive species-specific model, based on species planted proportions with DE terms interacting with the proportion of H. maximiliani and the spatial pattern treatment was again the best model (Table 2, Appendix S1). In this case, including random pairwise interaction terms improved model fit (Table 1). Again, we had no evidence of the species-specific contributions to biomass being related to their functional identities.

Although the best-fit model was similar between years 2 and 3, predicted biomass yields from the year 3 model were generally lower relative to the year 2 model (Figure 3 vs. 4). In year 3, A. gerardii, S. rigida (as in year 2) and A. canadensis were predicted to benefit the most from increased intraspecific interactions under the aggregated species pattern treatment. Sorghastrum nutans was again predicted to suffer the most under the aggregated spatial pattern treatment (Figure 4a vs. 4b). Including an additional 20% of H. maximiliani was again predicted to improve the ability of R. columnifera to interact with other species and reduce the ability of D. canadense to interact with other species (Figure 4a vs. 4c).

4 | DISCUSSION

We used Diversity-Interactions models to quantify diversity effects in each of the first three years of a grassland biodiversity experiment. Species interactions that contributed to diversity effects developed over time and differed among species. In the first growing season, aside from the most productive forb, H. maximiliani, species interacted equally to positively affect plot biomass. In the second growing season, each species contributed a unique constant to interactions that affected plot biomass. These species interaction constants were affected by H. maximiliani and the species planting pattern. This continued into the third growing season. In all three years, plot biomass was best described when species expected proportions were set based on their individual (planted) proportions. It appears that species interactions that form grassland diversity effects are affected by the fine-scale neighborships among species and can be modified in the presence of even a single, high-performing species. Our results suggest that managers need to consider species-specific responses, as opposed to species functional identities, when planning for diversity effects in species-rich reconstructed grasslands.

4.1 | Helianthus maximiliani effects

As in other studies (Dickson & Busby, 2009; Korbacheh, Jarchow, English, & Liebman, 2019; Nemec, Allen, Helzer, & Wedin, 2013;
Seahra et al., 2019), a productive Heliantheae forb initially dominated our experimental tallgrass prairies reconstructed on a former agricultural field. To address this statistically, we allowed diversity effects in our DI models to differ in *H. maximiliani* plots and treated these plots with a different variance structure. This additional statistical treatment and interpretation of *H. maximiliani* effects was biologically warranted. In the context of the SPaCE experiment, we previously reported that this species contributed to strong selection effects in the first and second growing seasons (McKenna & Yurkonis, 2016). In general, the early dominance of *H. maximiliani* in reconstructed grasslands has been correlatively attributed to strong competitive and potentially allelopathic effects on co-occurring species (Dickson & Busby, 2009; Kordbacheh et al., 2019; Macías, Torres, JoséM, Molinillo, & Castellano, 1996; Nemec et al., 2013). However, evidence of a direct effect on other species is lacking in the literature.

This improved, yet temporary, productivity likely comes from how Heliantheae forbs capture belowground resources within former agricultural fields. The related crop species *Helianthus annuus*, domesticated from North American *Helianthus* species, is deep rooted (reported up to 3 m), with a faster advance rate and better water use efficiency than comparable warm-season, cool-season, and legume crops (Canadell et al., 1996; Krupinsky, Tanaka, Merrill, Liebig, & Hanson, 2006; Stone, Goodrum, Jaafar, & Khan, 2001;
Anecdotally, these annual sunflowers are known to forage for nitrogen leached beyond the typical crop root zone and are planted to recover “lost” nitrogen in agricultural systems. What limited research exists supports this assertion (Canadell et al., 1996; Corbeels, Hofman, & Cleemput, 1998; López-Bellido, López-Bellido, Castillo, & López-Bellido, 2003; Moore & Peterson, 2007). Interestingly, in a North Dakota, USA row crop species rotation study, annual sunflower was the only nonlegume whose residue enhanced subsequent crops (Krupinsky et al., 2006), an effect potentially related to higher leaf nutrient content (Fässler et al., 2010). It is possible that the increased *H. maximiliani* productivity in our study resulted from this greater, more rapid nitrogen and soil water acquisition from deeper in the soil profile. Wang’s (2008) work in similar North Dakota, USA grasslands also appears to support this assertion in that *H. maximiliani* had high root decomposition and mixtures with *H. maximiliani* had greater root decomposition than those without. Although we did not sample soil or plant tissue nutrients, growing season soil moisture was approximately 4% higher in *H. maximiliani* mixtures relative to non-*H. maximiliani* mixtures in all three years (2012 $F_{1,88} = 4.29, p < .05$; 2013 $F_{1,88} = 3.40, p = .07$; 2014 $F_{1,88} = 3.62, p = .06$; methods described in McKenna & Yurkonis, 2016).
Given its potential contribution to the water and nutrient balance of an entire plot, it makes sense that *H. maximiliani* altered interactions among the remaining species. Our results imply that its dominance early in the reconstruction process should be interpreted with caution in that high *H. maximiliani* biomass production does not necessarily result in detrimental effects to other species. Future studies need to consider its role in accessing belowground resources in the restoration context and its use in regulating nutrient dynamics in grassland agroecosystems.

### 4.2 Spatial pattern effects

As with others (Lamošová et al., 2010; Seahra et al., 2016; Stoll & Prati, 2001), we found that aggregating plant species at submeter scales alters grassland species interactions, particularly among subordinate, less productive species. When using ANOVA type approaches to analyze this data, we previously identified a weak overall effect of species pattern on biomass production and no diversity effect as determined by the Additive Partitioning BEF analysis method (McKenna & Yurkonis, 2016). While this net effect is useful from a total biomass production perspective, the approach used here demonstrates the value of DI models to highlight species-specific spatial pattern effects on diversity effects. With this analysis, *A. gerardii*, *S. rigidia*, and *S. nutans* were predicted to be most consistently affected by species planting pattern, but in varying ways. These varied effects may be due to differences in how species interact with local resources and their soil biota under different planting arrangements (McKenna, Darby, & Yurkonis, 2019; Schnitzer et al., 2011; Temperton, Mwangi, Scherer-Lorenzen, Schmid, & Buchmann, 2007; Van der Putten et al., 2013). While we were unable to determine the mechanisms behind these predicted species-specific responses to species patterns, the DI modeling framework was useful for identifying which species should be further considered when applying these findings in a restoration context.

### 4.3 Planted versus realized proportions

From our study, it appears that using species planted proportions is sufficient for characterizing diversity effects in the DI framework for reconstructed grassland communities. It is well documented that diversity effects are sensitive to variation in species yields (Fargione et al., 2007; Polley, Wilsey, & Derner, 2003) that arise from biotic (i.e., plant-soil feedbacks) and abiotic sources (i.e., changes in resource availability, variation in plant phenology at harvest). These factors can change the rank-order among species and their proportional contributions to mixtures among years without affecting species interactions that affect community biomass (Loreau & Hector, 2001). For example, in our study, *S. rigidia* did not bolt from the basal rosette stage prior to harvest in year 1, but did so prior to harvest in years 2 and 3. This affected the proportion of *S. rigidia* in mixture among years, but likely bore little effect on how *S. rigidia* interacted with others within each growing season. *Helianthus maximiliani* and *A. canadensis* had similar swings in their biomass that likely did not affect how they interacted with other species over time. Although species biomass proportions have been used to improve DI models in communities with less variation among species and greater temporal stability (Fibich et al., 2015; Finn et al., 2013), it appears that this is ineffective for predicting peak biomass in communities with high variation among species and over time. This is especially important given that there is such a high labor cost to obtaining annual species-specific yield data, which were ultimately less informative.

### 4.4 Tallgrass prairie diversity effects

In applying DI models to species-rich tallgrass prairies, we expand upon a developing literature on species-specific grassland diversity effects, and affirm that species-specific interactions drive diversity effects in species-rich grasslands. Diversity-Interactions models were first applied to assess biomass production in a pasture experiment seeded with two grasses and two legumes. Given the small and relatively similar species pool, it was not surprising that the average pairwise model (M2) was consistently the best-fit model for this agroecosystem (Finn et al., 2013; Kirwan et al., 2007). In applying DI models to assess biomass production within a nine-species grassland experiment, Brophy, Dooley, et al. (2017) found that more complex species-specific interactions (e.g., functional group with random pairwise interaction) contributed to grassland diversity effects. We affirm this finding in that M3 consistently best explained plot biomass with an even larger species pool. These results indicate that while diversity effects exist, potential species contributions must be evaluated on a species-by-species basis when planning for emergent grassland diversity effects in the grassland reconstruction process.

### 4.5 Management implications

The findings have implications for grassland reconstruction efforts. First, it is clear that multiple species are needed to maximize diversity effects in reconstructed tallgrass prairies. While many studies have demonstrated this effect (Cardinale et al., 2007; Isbell, Polley, & Wilsey, 2009; Seahra et al., 2016), our study is unique in that we quantified specific species contributions to diversity effects. Specifically, we found that including *H. maximiliani* can enhance diversity effects, albeit it can appear that it outcompetes others based on its initially high biomass production (Dickson & Busby, 2009; Kordiachae et al., 2019; Nemec et al., 2013). Second, because species broad functional identities (cool-season, warm-season, forb, legume) were not informative, managers may best approach planning for tallgrass prairie diversity effects by keeping individual species characteristics, as opposed to their broad functional identities, in mind. Finally, it is necessary for managers to take a species-specific approach to planning planting activities in order to take advantage of the benefits of aggregating select species (e.g., *S. rigidia*, *A. gerardii*).

### ACKNOWLEDGMENTS

We thank R. Sheppard, K. Drees, M. Flom, members of the UND Grassland Ecology Lab, volunteers from the UND Biology
Author's Contributions

KAY and TPM designed and established the experiment. TPM coordinated data collection. CB and JM designed the data analysis methods. CB and JM analyzed the data with contributions from KAY and TPM. TPM, KAY, and CB wrote the manuscript with assistance from JM.

Data Availability Statement

Data used for the analysis in this manuscript are available in the Dryad Repository: https://doi.org/10.5061/dryad.r2h6h33

ORCID

Thomas P. McKenna https://orcid.org/0000-0001-6531-3452

Conflict of Interest

None declared.

References

Brophy, C., Dooley, Á., Kirwan, L., Finn, J. A., McDonnell, J., Bell, T., ... Connolly, J. (2017). Biodiversity and ecosystem function: Making sense of numerous species interactions in multi-species communities. Ecology, 98(7), 1771–1778. https://doi.org/10.1002/ecy.1872

Brophy, C., Finn, J. A., Lüschker, A., Suter, M., Kirwan, L., Sebastià, M.-T., ... Connolly, J. (2017). Major shifts in species’ relative abundance in grassland mixtures alongside positive effects of species diversity in yield: A continental-scale experiment. Journal of Ecology, 105(5), 1210–1222. https://doi.org/10.1111/1365-2745.12754

Canell, J., Jackson, R. B., Ehleringer, J. J., Mooney, H. A., Sala, O. E., & Schulze, E.-D. (1996). Maximum rooting depth of vegetation types at the global scale. Oecologia, 108(4), 583–595. https://doi.org/10.1007/BF00329030

Cardinale, B. J., Wright, J. P., Cadotte, M. W., Carroll, I. T., Hector, A., Srivastava, D. S., ... Weis, J. J. (2007). Impacts of plant diversity on biomass production increase through time because of species complementarity. Proceedings of the National Academy of Sciences of the United States of America, 104(46), 18123–18128. https://doi.org/10.1073/pnas.0709069104

Connolly, J., Bell, T., Bolger, T., Brophy, C., Carnus, T., Finn, J. A., ... Weigelt, A. (2013). An improved model to predict the effects of changing biodiversity levels on ecosystem function. Journal of Ecology, 101(2), 344–355. https://doi.org/10.1111/j.1365-2745.12052

Connolly, J., Sebastià, M.-T., Kirwan, L., Finn, J. A., Lurba, R., Suter, M., ... Lüschker, A. (2018). Weed suppression greatly increased by plant diversity in intensively managed grasslands: A continental-scale experiment. Journal of Applied Ecology, 55(2), 852–862. https://doi.org/10.1111/1365-2664.12991

Corbeels, M., Hofman, G., & Van Cleemput, O. (1998). Residual effect of nitrogen fertilisation in a wheat–sunflower cropping sequence on a Vertisol under semi-arid Mediterranean conditions. European Journal of Agronomy, 9(2), 109–116. https://doi.org/10.1016/S1161-0301(98)00030-6

Dickson, T. L., & Busby, W. H. (2009). Forb species establishment increases with decreased grass seeding density and with increased forb seeding density in a northeast Kansas, U.S.A., experimental prairie restoration. Restoration Ecology, 17(5), 597–605. https://doi.org/10.1111/j.1526-100X.2008.00427.x

Fargione, J., Tilman, D., Dybzinski, R., Lambers, J. H. R., Clark, C., Harpole, W. S., ... Loreau, M. (2007). From selection to complementarity: Shifts in the causes of biodiversity–productivity relationships in a long-term biodiversity experiment. Proceedings of the Royal Society B: Biological Sciences, 274(1611), 871–876. https://doi.org/10.1098/rspb.2006.0351

Fässler, E., Robinson, B. H., Stauffer, W., Gupta, S. K., Papritz, A., & Schulin, R. (2010). Phyto management of metal-contaminated agricultural land using sunflower, maize and tobacco. Agriculture, Ecosystems & Environment, 136(1), 49–58. https://doi.org/10.1016/j.agee.2009.11.007

Fibich, P., Rychtecká, T., & Lepl, J. (2015). Analysis of biodiversity experiments: A comparison of traditional and linear-model-based methods. Acta Oecologica, 63, 47–55. https://doi.org/10.1016/j.actao.2015.02.002

Finn, J. A., Kirwan, L., Connolly, J., Sebastià, M. T., Helgdottir, A., Baadshaug, O. H., ... Lüschker, A. (2013). Ecosystem function enhanced by combining four functional types of plant species in intensively managed grassland mixtures: A 3-year continental-scale field experiment. Journal of Applied Ecology, 50(2), 365–375. https://doi.org/10.1111/1365-2664.12041

Grace, J. B., Keough, J., & Guntenspergen, G. R. (1992). Size bias in traditional analyses of substitutive competition experiments. Oecologia, 90(3), 429–434. https://doi.org/10.1007/BF00317702

Hector, A., Bell, T., Connolly, J., Finn, J., Fox, J., et al. (2009). The analysis of biodiversity experiments: From pattern toward mechanism. In S. Naheem, D. E. Bunker, A. Hector, M. Loreau, & C. Perrings (Eds.), Biodiversity, ecosystem functioning, and human wellbeing: An ecological and economic perspective (pp. 94–104). New York, NY: Oxford University Press.

Houseman, G. R. (2014). Aggregated seed arrival alters plant diversity in grassland communities. Journal of Plant Ecology, 7(1), 51–58. https://doi.org/10.1093/jpe/rtt044

Isbell, F., Polley, H. W., & Wilsey, B. (2009). Species interaction mechanisms maintain grassland plant species diversity. Ecology, 90(7), 1821–1830. https://doi.org/10.1890/08-0514.1

Kirwan, L., Connolly, J., Finn, J. A., Brophy, C., Lüschker, A., Nyfeler, D., & Sebastià, M.-T. (2009). Diversity-interaction modeling: Estimating contributions of species identities and interactions to ecosystem function. Ecology, 90(8), 2032–2038. https://doi.org/10.1890/08-1684.1

Kirwan, L., Lüschker, A., Sebastià, M. T., Finn, J. A., Collins, R. P., Porqueddu, C., ... Connolly, J. (2007). Evenness drives consistent diversity effects in intensive grassland systems across 28 European sites. Journal of Ecology, 95(3), 530–539. https://doi.org/10.1111/j.1365-2745.2007.01225.x

Kordbacheh, F., Jarchow, M., English, L., & Liebman, M. (2019). Productivity and diversity of annually harvested reconstructed prairie communities. Journal of Applied Ecology, 56(2), 330–342. https://doi.org/10.1111/1365-2664.13267

Krupinsky, J. M., Tanaka, D. L., Merrill, S. D., Liebig, M. A., & Hanson, J. D. (2006). Crop sequence effects of 10 crops in the northern Great Plains. Agricultural Systems, 88(2), 227–254. https://doi.org/10.1016/j.agsy.2005.03.011
Lamošová, T., Doležal, L., Lanta, V., & Lepš, J. (2010). Spatial pattern affects diversity–productivity relationships in experimental meadow communities. Acta Oecologica, 36(3), 325–332. https://doi.org/10.1016/j.actao.2010.02.005

López-Bellido, R. J., López-Bellido, L., Castillo, J. E., & López-Bellido, F. J. (2003). Nitrogen uptake by sunflower as affected by tillage and soil residual nitrogen in a wheat–sunflower rotation under rainfed Mediterranean conditions. Soil and Tillage Research, 72(1), 43–51. https://doi.org/10.1016/S0167-1987(03)00048-5

Loreau, M., & Hector, A. (2001). Partitioning selection and complementarity in biodiversity experiments. Nature, 412(6842), 72–76. https://doi.org/10.1038/35083573

Macías, F. A., Torres, A., JoséM, G., Molinillo, R. M. V., & Castellano, D. (1996). Potential allelopathic sesquiterpene lactones from sunflower leaves. Phytochemistry, 43(6), 1205–1215. https://doi.org/10.1016/S0031-9422(96)00392-5

McKenna, T. P., Darby, B. J., & Yurkonis, K. A. (2019). Effects of monoculture-conditioned soils on common tallgrass prairie species productivity. Journal of Plant Ecology, 12(3), 474–484. https://doi.org/10.1093/jpe/ryt040

McKenna, T. P., & Yurkonis, K. A. (2016). Across species-pool aggregation alters grassland productivity and diversity. Ecology and Evolution, 6(16), 5788–5795. https://doi.org/10.1002/ece3.2325

Moore, S. L., & Peterson, E. W. (2007). Transport and fate of nitrate within soil units of glacial origin. Environmental Geology, 52(8), 1527–1537. https://doi.org/10.1007/s00254-006-0597-2

Murrell, D. J. (2010). When does local spatial structure hinder competitive coexistence and reverse competitive hierarchies? Ecology, 91(6), 1605–1616. https://doi.org/10.1890/09-0832.1

Nemec, K. T., Allen, C. R., Helzer, C. J., & Wedin, D. A. (2013). Influence of richness and seeding density on invasion resistance in experimental tallgrass prairie restoration. Ecological Restoration, 31(2), 168-185. https://doi.org/10.3368/er.31.2.168

Polley, H. W., Wilsey, B. J., & Derner, J. D. (2003). Do species evenness and plant density influence the magnitude of selection and complementarity effects in annual plant species mixtures? Ecology Letters, 6(3), 248–256. https://doi.org/10.1046/j.1461-0248.2003.00422.x

Porensky, L., Porensky, K., Vaughn, T., & Young, T. P. (2012). Can initial intraspecific spatial aggregation increase multi-year coexistence by creating temporal priority? Ecological Applications, 22(3), 927–936. https://doi.org/10.1890/11-0818.1

Schnitzer, S. A., Klironomos, J. N., HilleRisLambers, J., Kinkel, L. L., Reich, P. B., Xiao, K., ... Scheffer, M. (2011). Soil microbes drive the classic plant diversity-productivity pattern. Ecology, 92(2), 296. https://doi.org/10.1890/10-0773.1

Seahra, S. E., Yurkonis, K. A., & Newman, J. A. (2016). Species patch size at seeding affects diversity and productivity responses in establishing grasslands. Journal of Ecology, 104(2), 479–486. https://doi.org/10.1111/1365-2745.12514

Seahra, S., Yurkonis, K. A., & Newman, J. A. (2019). Seeding tallgrass prairie in monospecific patches promotes native species establishment and cover. Restoration Ecology, 27(1), 82–91. https://doi.org/10.1111/rec.12715

Stoll, P., & Prati, D. (2001). Intraspecific aggregation alters competitive interactions in experimental plant communities. Ecology, 82(2), 319–327. https://doi.org/10.1890/0012-9658(2001)082[0319:IAAI|2.0.CO;2

Stone, L. R., Goodrum, D. E., Jaafar, M. N., & Khan, A. H. (2001). Rooting front and water depletion depths in grain sorghum and sunflower. Agronomy Journal, 93(5), 1105–1110. https://doi.org/10.2134/agronj2001.935110x

Stone, L. R., Goodrum, D. E., Schlegel, A. J., Jaafar, M. N., & Khan, A. H. (2002). Water depletion depth of grain sorghum and sunflower in the central high plains. Agronomy Journal, 94(4), 936–943. https://doi.org/10.2134/agronj2002.9360

Tempton, V. M., Mwangi, P. N., Scherer-Lorenzen, M., Schmid, B., & Buchmann, N. (2007). Positive interactions between nitrogen-fixing legumes and four different neighbouring species in a biodiversity experiment. Oecologia, 151(2), 190–205. https://doi.org/10.1007/s00442-006-0576-z

van der Putten, W. H., Bardgett, R. D., Bever, J. D., Bezemner, T. M., Casper, B. B., Fukami, T., ... Wardle, D. A. (2013). Plant-soil feedbacks: The past, the present and future challenges. Journal of Ecology, 101(2), 265–276. https://doi.org/10.1111/j.1365-2745.12054

Wang, J. (2008). The relationship between root decomposition and plant biodiversity. Streeter, ND: Central Grasslands Research Extension Center (CGREC).

Yurkonis, K. A., & McKenna, T. P. (2014). Aggregating species at seeding may increase initial diversity during grassland reconstruction. Ecological Restoration, 32(3), 275–281. https://doi.org/10.3368/er.32.3.275

**SUPPORTING INFORMATION**

Additional supporting information may be found online in the Supporting Information section at the end of the article.

*How to cite this article:* McKenna TP, McDonnell J, Yurkonis KA, Brophy C. *Helianthus maximiliani* and species fine-scale spatial pattern affect diversity interactions in reconstructed tallgrass prairies. *Ecol. Evol.* 2019;9:12171–12181. https://doi.org/10.1002/eco3.5696