Effect of the Rock Stress on the Water Jet Cutting Performance

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Abstract
Underground quarrying is rarely adopted for granite extraction due to the difficulties in the implementation of traditional technologies (drilling and explosive). As alternative to drilling and explosive, the combination of diamond wire and water jet seems to be the most promising available technology. The cutting performance achievable with the water jet technology depends on the operative parameters, the material characteristics and the state of stress within the rock massif. To assess the effect of the state of stress on the cutting rate, laboratory tests have been performed with an oscillating water jet machine on granite samples subjected to a static load. The stress distribution in the layer of rock to be removed has been evaluated by numerical simulation with the FLAC code (Fast Lagrangian Analysis of Continua). The correlation between the results of the cutting tests and the numerical models of the rock samples has been inferred. Starting from a conceptual model, which theoretically describes the relationship between the cutting rate and the stress, a step function was defined that indicates the ranges of stress where predefined values of the cutting rate are workable.

Keywords Oscillating water jet · Water jet performance · Rock state of stress · Granite underground quarrying

List of Symbols
\[\begin{align*}
\alpha & \quad \text{Angular amplitude of the lance oscillations (°)} \\
\beta & \quad \text{Angle of the jet impact on the rock surface (°)} \\
f & \quad \text{Lance oscillating frequency (Hz)} \\
S & \quad \text{Nozzle distance from the groove’s bottom surface (mm)} \\
p & \quad \text{Water jet generation pressure (Pa)} \\
\text{SOD} & \quad \text{Stand off distance (mm)} \\
v_t & \quad \text{Transverse velocity (m/min)} \\
a & \quad \text{Advancement per cycle (mm)} \\
d & \quad \text{Deepening per cycle (mm)} \\
\text{CR} & \quad \text{Cutting rate (m²/h)} \\
\text{CR}^* & \quad \text{Predefined cutting rate (m²/h)} \\
\text{ECR} & \quad \text{Equilibrium cutting rate (M²/h)} \\
\sigma_{xx} & \quad \text{Normal stress component in x direction (Pa)} \\
\Delta\sigma_{xx} & \quad \text{Normal stress interval (Pa)} \\
\sigma_{xx} & \quad \text{Sustainability limit stress (Pa)} \\
E\sigma_{xx} & \quad \text{Efficiency limit stress (Pa)}
\end{align*}\]

1 Introduction
Surface quarrying is the most common method to extract dimensional stones, due to the relatively low depth of the deposits, as well as to the objective difficulties in implementing traditional cutting technologies in underground environments. On the other hand, new constraints are progressively imposed by national and international environmental regulation which affect the overall economic balance of the industrial enterprise. As a matter of fact, underground quarrying appears to be better suited to modern trends, as it minimizes the temporary negative effects due to the project actions, such as noise (Bortolussi 2010) and emission of air pollutants (Particulate Matter, in particular), as well as the permanent effects of the quarry itself, among which land consumption and landscape alteration are the most significant (Dentoni 2020; Babitha 2007; Fugiel 2017).

At the present time, underground quarrying is widely diffused in the marble extraction industry, while it is rarely adopted for granite extraction (Fornaro 1992). In fact, while marble cutting technologies (wire and diamond saw) are suited both for surface and underground excavation, the
technologies traditionally used for granite extraction (drilling and explosive) (Ashmole 2008) can be hardly implemented underground.

As alternative to drilling and explosive, granite slotting can be performed with the diamond wire machine, which yet needs the support of an another technology due to its inherent limitations: the combination of diamond wire and water jet seems to be the most promising solution, with the water jet playing the same role as the diamond saw in marble quarries (Ciccu and Fiamminghi 1996).

The use of the water jet technology in mining and quarrying has been proposed by many authors for its ability to reduce the production of dust, the temperature of the mechanical tools when hydro-mechanical excavation technologies are used and, in general, of extending mechanical excavation to the hard and abrasive rocks (Averin 2017; Hood 1993).

The experimental study hereby discussed is the development of a research program started before 2000, which has been implemented with new procedures and additional laboratory tests (Ciccu 2013); it specifically deals with the application of the oscillating water jet technology to underground extraction of granite and intends to investigate the correlation between the rock’s state of stress and the water jet’s cutting performance. In fact, some industrial experiences have demonstrated as the achievable slotting rate on a given type of rock depends on the state of stress within the rock massif (Stoxreiter 2018): it has been observed that in compressed rocks, the attainable cutting rate is lower than in unstressed rocks, whereas it is higher in rocks subjected to tensile stresses (Ciccu 1998).

This article reports the results of the cutting tests performed on granite samples of Rosa Beta quarried in Sardinia (Italy); three conditions have been investigated: unloaded samples (reference condition), samples subjected to compressive stress and samples subjected to tensile stress. The stress distribution in the layers of rock being cut has been modeled with the three-dimensional FLAC code, for the three experimental conditions under investigation. Two distinct yet complementary issues were taken into consideration: the relationship between the cutting rate and the state of stress within the rock and its dependence on the water jet energy.

2 Underground Quarrying with Water Jet

2.1 Combination of Diamond wire and Water Jet

A suitable diamond wire–water jet combination for underground extraction of granite is illustrated in Fig. 1, which shows the two phases of a cutting sequence aimed at isolating 8 commercial blocks. To cut the side faces of the blocks, a 3 m pilot hole is first drilled perpendicular to the front, from which a first slot can be started. The water jet lance, which supports and directs the nozzle towards the rock to be removed, moves forth and back, starting from the pilot hole and proceeding parallel to it. After each cycle (two strokes) the lance is moved sideways, by incremental steps, thus progressively extending the first slot’s surface.

All subsequent slots can be started from the first, following a convenient order (first phase). Once all the side slots are completed, individual blocks can be extracted by cutting the back faces with the diamond wire machine (second phase): two vertical cuts in the example of Fig. 1 are required to obtain blocks of proper width (1.5 m).
2.2 Slotting with Oscillating Water Jet

In the oscillating version of the water jet technology, the lance that holds the nozzle is animated by an oscillatory motion around its own axis (frequency $f$ and angular amplitude $\alpha$) and a transverse motion (velocity $v_t$) in the direction of the groove generated by the jet itself (in z-direction) (Reichman 1978). The nozzle is located at a given distance $S$ (in y-direction) from the groove’s bottom surface, upon which the jet impacts with a fixed angle $\beta$ (the standoff distance is the distance from the nozzle to the jet impact point, along the direction defined by $\beta$ (Fig. 2)). A simplified 3D representation of the operating parameters above described is reported in Fig. 3.

The lance travels along the groove in both directions alternately: one cycle (two strokes) generates the increment $d$ of the groove depth (deepening); at each cycle the lance is approached to the groove’s bottom by a distance $a$. The excavation performance is given by the areal cutting rate $CR$, which is the product of the lance’s transverse velocity $v_t$ by the number of cycle in the unit of time by the lance’s advancement $a$. The cut efficiency is expressed by the amount of energy required to remove the rock unit volume (J/cm$^3$) (Summers 1991; Bortolussi 1992).

For a given rock and constant transverse velocity, the cut develops in steady conditions when the groove’s deepening $d$ equals the lance’s advancement $a$; under those conditions, the standoff distance (SOD) remains constant (i.e., equal to the optimal set-up value). If the lance’s transverse velocity is too high, the cut’s deepening becomes lower than the lance’s advancement and SOD progressively decreases, until the lance collides with the bottom of the groove. If the lance’s transverse velocity is too low, the cut deepening becomes greater than the lance’s advancement and a progressive increase of SOD occurs; this corresponds to a reduction of both the cutting efficiency and the cut’s deepening, which goes on until $d$ equals $a$ again; from this point onwards, the

Fig. 2 Geometric parameters of the water jet in the yz plane

Fig. 3 Operating parameters of the oscillating water jet: frequency $f$ and angular amplitude $\alpha$ (lance’s oscillating motion); velocity $v_t$ (lance’s transverse motion); distance $S$ from the nozzle to groove’s bottom surface
cut proceeds in steady conditions, with a SOD greater than the optimum set-up value and both the efficiency and the cutting rate CR lower than maximum attainable (Hood et al. 1990; Rehbinder 1977).

In compressed rocks, the reduction of the resisting cross-sectional area due to the slot’s development generates a progressive increase of the compressive stress acting at the groove’s bottom and a corresponding progressive reduction in the cut’s deepening $d$: a geometric limit condition is reached, beyond which $d$ becomes greater than $a$; from this point onwards, the continuation of the cut with the same transverse velocity can only take place by reducing the lance’s advancement in accordance to the decrease of the cut’s deepening, with a corresponding reduction of the cutting rate.

In tense rocks, the reduction of the resisting cross-sectional area due to the cut’s advancement generates a progressive increase of the tensile stress acting at the groove’s bottom and a corresponding progressive increase of the cut deepening, up to the limit beyond which $d$ becomes greater than $a$; from this point onwards, the continuation of the cut with the same transverse velocity and at the maximum efficiency requires the increasing of the lance’s advancement, with corresponding increment of the cutting rate.

According to the forethoughts above, the stress limit condition is defined as that stress beyond which the maintenance of the optimal SOD implies the modification of CR: a reduction in case of compression stress and a raise in case of tensile stress. In compressed rocks and for a given CR, the stress limit condition represents the value of the stress up to which the rock can be cut and beyond which the CR must be reduced. In tense rocks and for a given CR, it represents the level of stress up to which the rock is cut with the maximum efficiency and beyond which the CR has to be increased to preserve the efficiency level.

It is worth noticing that CR can be modified by adjusting either the lance’s advancement $a$ or the lance’s transverse velocity $v_x$. In the experimental test described in the following sections of the article, CR has been modified by adjusting $v_x$; higher values were used to reduce CR and lower values to increase CR, with a fixed value of the lance’s advancement $a$.

### 2.3 State of Stress in Underground Quarrying

In underground production of squared blocks, the first excavation phase consists of the opening of an entry tunnel, starting from the hillside, until the planned quarrying area is reached; then the tunnel is further enlarged leaving the pillars to support the roof. In case of thick deposits, the excavation can be further developed below the level of the access tunnel: a large chamber is progressively created by exploiting the rock layers with a downwards sequence.

The compression vertical component of the original stress acting in the rock can be quite high, depending of the tunnel depth; during the tunnel advancement, its value at the bottom of the horizontal grooves realized to extract the rock blocks is further increased as a result of the vertical stress redistribution. The same phenomenon occurs at the chambers’ walls during their enlargement. As a result of the extraction of the first layer of the chamber (roof layer), the compression stress in the rock volume below is almost thoroughly relieved. Consequently, during the following cutting operations, the stress at the bottom of the grooves is significantly lowered.

Tensile states of stress typically occur at the chamber roof, as a function of the roof span and the ratio ($k$) between the horizontal and vertical stress components ($k = \sigma_h/\sigma_v$). In the typical geometric configurations of underground quarries it is rare to cut blocks subjected to tensile stress; on the other hand, based on the research results, tensile stress could be artificially generated to improve the water jet slotting performances.

### 3 The Experimental Research

#### 3.1 Rock Samples and Experimental Set-up

Three series of cutting tests have been performed on granite specimens of Rosa Beta quarried in Sardinia (Italy), first unstressed and then subjected to compression and tensile stresses, aimed at evaluating the stress limit condition at which a predefined cutting rate can be maintained. The experiments have been repeated for three jet generation pressures (100, 160 and 200 MPa).

The physical and mechanical properties of the granite samples are synthesized in Table 1.

The experimental set-up installed at the Water Jet laboratory of DICAAR (Department of Civil and Environmental Engineering and Architecture), in Cagliari University (Italy), consists of the following components:

- a Hammelmann High-Pressure plunger pump (power at the engine flywheel: about 300 kW; maximum flowrate: 54 l/min at 250 MPa);

| Property                             | Value |
|--------------------------------------|-------|
| Bulk specific gravity [kg/m³]        | 2.588 |
| Absorption coefficient [%]           | 4.85  |
| Porosity [%]                         | 0.63  |
| Compressive strength [MPa]           | 192   |
| Flexural strength (MPa)              | 156   |
| Impact test (Height of fall) [cm]    | 68    |
| P-wave velocity [m/s]                | 5626  |
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– an oscillating lance (top frequency: \( f = 20 \) Hz; maximum traverse velocity \( v_t \): 15 m/min);
– a block carrier platform;
– a programmable lance control unit;
– a specially designed uniaxial compression cell provided with a hydraulic jack capable of imparting a load up to 100 t.

Table 2 reports the operative parameters of the oscillating water jet. Figure 4 represents the water jet lance and its slotting action on an unloaded sample.

### 3.2 Test on Unloaded Samples

The first test series has been performed on unloaded samples, aimed at assessing the reference cutting rate at the zero stress condition. In this case, the deepening of the cut does not cause any change in the state of stress within the rock, so that \( CR \) only depends on the material properties and the water jet operative parameters. The maximum value of \( CR \) is estimated by adjusting the lance’s transverse velocity as to obtain the equivalence between the cut’s deepening \( d \) and the lance’s advancement \( a \). Table 3 reports the experimental plan for the unloaded samples.

### 3.3 Test on Compressed Samples

The second series of test has been carried out by subjecting the granite samples to an evenly distributed lateral compression, according to the scheme in Fig. 5: in that condition, the slot progress causes the increment of the compression stress in the layer of rock where the jet acts (grove’s bottom), so that a progressive reduction of the cutting rate is required. Table 4 reports the succeeding values of the cutting rates

**Table 2** Water jet operative parameters

| Parameter                                      | Value       |
|-----------------------------------------------|-------------|
| Water jet generation pressure [MPa]           | 100, 160, 200 |
| Nozzle diameter \( \Phi \) [mm]                | 0.96        |
| Stand-off distance SOD [mm]                    | 20          |
| Jet impact angle \( \beta \) [°]               | 50°         |
| Oscillation frequency \( f \) [Hz]             | 20 Hz       |
| Sweeping angle \( \alpha \) [°] on each side   | 22°         |
| Advancement per cycle [y-direction] \( a \) [mm] | 2           |
| Transverse velocity [z-direction] \( v_t \) [m/min] | variable   |

**Table 3** Experimental plan for unloaded samples

| Test | Sample No | Load (kN) | Jet pressure \( p \) (MPa) | Advancement \( a \) (mm) |
|------|------------|-----------|----------------------------|--------------------------|
| Z1   | Z1a, Z1b, Z1c | 0         | 100                        | 2                        |
| Z2   | Z2a, Z2b, Z2c | 0         | 160                        | 2                        |
| Z3   | Z3a, Z3b, Z3c | 0         | 200                        | 2                        |

Fig. 4 Water jet lance (left) and slotting of an unloaded sample (right)
(CR*) to be adopted during the test, which were determined after some preliminary trials.

Aimed at evaluating the limit slot depth (i.e., maximum depth up to which a predetermined cutting rate CR* can be maintained), the test starts at the highest suitable CR for a given water jet generation pressure (e.g., 0.45 m²/h with \( p = 100 \) MPa) and is then carried out to the depth at which a reduction of SOD can be observed. To this purpose, at each stroke the lance is stopped and the distance between the nozzle and the mean plane of the slot bottom is measured. At that point, CR is lowered to the subsequent predefined value (CR* = 0.36 m²/h) and the cut continues until a new decrease of SOD becomes apparent. Again CR is dropped to the lower consistent value (CR* = 0.30 m²/h) to proceed with the cut on the same slot. The test ends when the limit slot depth is reached with the lowest CR* in the experimental plan. The procedure above described has been followed to perform the experimental test with applied lateral loads of 250 and 500 kN. Six granite samples were used for each jet generation pressure. The lance’s advancement \( a \) was fixed at 2 mm and the cutting rate was adjusted by modifying the lance’s traverse velocity. The experimental plan for compressed samples is reported in Table 5.

### 3.4 Test on Tense Samples

With the third series of test, the alleged favorable effect of the tensile stress was investigated by applying a flexural load, as illustrated in Fig. 6. Two different load conditions were taken into consideration: \( F = 50 \) kN and \( F = 100 \) kN (total force acting on the sample), with a water jet generation pressure of 100 MPa. According to the experimental plan in Table 6, two cutting rates were selected for each load condition: 0.69 and 0.73 m²/h for \( F = 50 \) kN; 0.84 and 1.0 m²/h for \( F = 100 \) kN. As for the case of compressed samples, the lance’s advancement \( a \) was kept unchanged (2 mm per cycle) and the cutting rate progressively adjusted by modifying the lance’s transverse velocity \( v_t \).

Because the progress of the slot causes a growth in the tensile stress, the cut is started at the predefined lowest value of CR* and continues until the first increment of SOD is registered. The cutting rate is then raised up to the next step and the test continues.

### 3.5 Test Results

Test on the unloaded samples is meant to estimate the maximum obtainable cutting rate for each jet generation pressure \( (p = 100, 160, 200 \text{ MPa}) \). The resulting CRs are assumed as reference values for the analysis of the alterations induced by the state of stress. For each water jet generation pressure, Table 7 reports the optimum values of the transverse velocity \( v_t \) and the cutting rate CR, expressed as average of the three tests (a, b, c).

![Fig. 5 Loading condition for testing compressed samples (dimensions in cm)](image)

### Table 4 Cutting rate steps for compressed samples

| Water jet generation pressure, \( p \) (MPa) | Cutting rate steps, \( CR_\ast \) (m²/h) |
|------------------------------------------|------------------------------------|
| 100                                     | 0.45–0.36–0.30                     |
| 160                                     | 1.30–1.10–0.90–0.85                |
| 200                                     | 1.79–1.78–1.75–1.65                |

### Table 5 Experimental plan for compressed samples

| Test | Sample N° | Load (kN) | Jet pressure, \( p \) (MPa) | Traverse velocity, \( v_t \) (m/min) | Advance- ment \( a \) (mm) | Cutting rate, \( CR_\ast \) (m²/h) |
|------|-----------|-----------|-----------------------------|--------------------------------------|--------------------------|----------------------------------|
| C1   | C1a, C1b, C1c | 250       | 100                         | 3.75–3.0–2.5                         | 2                        | 0.45–0.36–0.30                   |
| C2   | C2a, C2b, C2c | 500       | 100                         | 3.75–3.0–2.5                         | 2                        | 0.45–0.36–0.30                   |
| C1’  | C1’a, C1’b, C1’c | 250       | 100                         | 10.83–9.17                           | 2                        | 1.30–1.10                        |
| C2’  | C2’a, C2’b, C2’c | 500       | 160                         | 7.50–7.08                            | 2                        | 0.90–0.85                       |
| C1’’ | C1’a, C1’b, C1’c | 250       | 200                         | 14.9–14.8                            | 2                        | 1.79–1.78                       |
| C2’’ | C2’a, C2’b, C2’c | 500       | 200                         | 14.6–13.7                            | 2                        | 1.75–1.65                       |
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The results of the experimental test on compressed samples are reported in Table 8, again in terms of mean value.

To test on samples subjected to tensile stress is meant to estimate the limit slot depths at which CR* must be increased, to maintain the original level of efficiency. Table 9 reports the results of the experimental test carried out on tensile samples with a jet generation pressure of 100 MPa. In Fig. 7, an example of the grooves generated by the water jet is given.

### 3.6 State of Stress Simulation

The stress distribution in the layer of rock being cut (groove’s bottom) has been analyzed using the three-dimensional FLAC (Fast Lagrangian Analysis of Continua) code.

#### Table 6 Experimental plan for tense samples

| Sample N° | Flexural load (kN) | Jet pressure \( p \) (MPa) | Traverse velocity \( v_t \) (m/min) | Advance-ment \( a \) (mm) | Cutting rate \( CR^* \) (m²/h) |
|-----------|-------------------|-----------------|-----------------|-------------|------------------|
| T1        | T1a T1b T1c       | 50              | 100             | 5.75–6.08   | 2                | 0.69–0.73         |
| T2        | T2a T2b T2c       | 100             | 100             | 7.00–8.33   | 2                | 0.84–1.00         |

#### Table 7 Results of test on unloaded samples

| Test | Samples | Jet pressure \( p \) (MPa) | Traverse velocity \( v_t \) (m/min) | Advance-ment \( a \) (mm) | Cutting rate \( CR^* \) (m²/h) |
|------|---------|-----------------|-----------------|-------------|------------------|
| Z1   | Z1a Z1b Z1c | 100             | 5.25=(5.5+4.9+5.2)/3 | 2            | 0.63             |
| Z2   | Z2a Z2b Z2c | 160             | 11.7=(11.0+12.5+11.5)/3 | 2            | 1.40             |
| Z3a  | Z3b Z3c   | 200             | 15.1=(14.8+15.0+15.3)/3 | 2            | 1.84             |

#### Table 8 Results of test on compressed samples

| Test          | Jet pressure \( p \) (MPa) | Lateral load (kN) | Cutting rate \( CR^* \) (m²/h) | Limit slot depth (mm) |
|---------------|-----------------|-----------------|-----------------|------------------|
| C1 (a, b, c)  | 100             | 250             | 0.45            | 25=(24.5+26+25)/3 |
|               |                 |                 | 0.36            | 35=(36+33.5+35)/3 |
|               |                 |                 | 0.30            | 60=(58+61+60.5)/3 |
| C2 (a, b, c)  | 100             | 500             | 0.45            | 8=(7.5+9+8)/3    |
|               |                 |                 | 0.36            | 15=(13.5+15+16)/3|
|               |                 |                 | 0.30            | 25=(27+25+24)/3  |
| C1 (a’, b’, c’) | 160            | 250             | 1.30            | 23=(22.5+24+22)/3|
|               |                 | 250             | 1.10            | 61=(60+63+60.5)/3|
| C2 (a’, b’, c’) | 160            | 500             | 0.90            | 44=(45+44+42)/3  |
|               |                 | 500             | 0.85            | 64=(63.5+65+64)/3|
| C1(a”, b”, c”) | 200            | 250             | 1.79            | 40=(41+40+39)/3  |
|               |                 | 250             | 1.78            | 65=(63,5+66+64)/3|
| C2 (a”, b”, c”) | 200            | 500             | 1.75            | 65=(66+63+65)/3  |
|               |                 | 500             | 1.65            | 82=(81+83+82.5)/3|

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Fig. 6 Loading condition for testing tense samples (dimensions in cm)
Two three-dimensional models were built, CM and TM, subjected to compressive and tensile stress, respectively. The spatial orientation of the models is set as follows:

- **Z-direction**: axis of the slot.
- **Y-direction**: depth of the slot.
- **X-direction**: perpendicular to the slot plane.

The two models represent a 5 cm thick slice of the sample (along the z-direction), as indicated in Fig. 8. The stress acting in the volume removed by the water jet at each cycle is calculated as average of the normal components ($\sigma_{xx}$) acting on the elements of the calculation grid included in 2 mm of thickness (Fig. 9).

The rock material has been modeled as linear elastic, considering the physical and mechanical properties of Rosa Beta reported in Table 1. The state of stress was calculated for each of the experimental limit configurations (i.e.: experimental limit depths).

### Table 9 Test on tenses samples—p = 100 MPa—Results

| Test   | Flexural load (kN) | Cutting rate $CR^*$ (m²/h) | Limit slot depth (mm) |
|--------|---------------------|-----------------------------|------------------------|
| T1 (a, b, c) | 50                  | 0.69                        | 5 (4.5 + 6 + 5)/3      |
|         |                     | 0.73                        | 30 (30.5 + 29.6 + 29.8)/3 |
| T2 (a, b, c) | 100                 | 0.84                        | 30 (30.1 + 29.2 + 30.7)/3 |
|         |                     | 1.00                        | 50 (51 + 48.5 + 49)/3   |

### 4 Discussion

#### 4.1 Research Objective and Assumptions

The experimental research hereby discussed is meant to define the dependence of the cutting rate $CR$ on the stress component $\sigma_{xx}$ acting in the volume of rock to be removed. If, for a given value $\sigma_{xx}$, the *Equilibrium Cutting Rate* $ECR$ indicates the value of the cutting rate at which neither an increase nor a reduction of $SOD$ is observable, the continuous curve in Fig. 10 conceptually describes the relationship.
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The effect of the rock stress on the water jet cutting performance is studied, with a focus on the relationship between the cutting rate (CR) and the normal stress component (σ_{xx}).

The cutting tests are performed along the yz plane in a rock subjected to compressive stress. The cutting rate is reduced to CR2, as the new value σ_{xx1} of the compressive stress (σ_{xx} for CR2) is the Eσ_{xx} (CR2) = σ_{xx1}). The cut proceeds up to the end (Z = Z3) with CR = CR3.

The diagram of Fig. 11 summarizes the relationships between the deepening of the groove in the rock mass (increase of Z), the change in the σ_{xx} (Z) stress component acting within the volume of rock to be removed and the cutting rate CR(σ_{xx}).

The figure shows three succeeding steps of a cut performed along the yz plane in a rock subjected to compressive stress.

**STEP1.** The initial value of the normal stress component is σ_{xx0}, which is also the Efficiency limit stress (Eσ_{xx}) for the first preset value of the cutting rate CR1 (Eσ_{xx} (CR1) = σ_{xx0}). As the cut proceeds from Z0 to Z1, the compressive stress component σ_{xx} progressively increases up to the value σ_{xx1}, which corresponds to the Sustainability Limit Stress (Sσ_{xx}) for the first preset value of the cutting rate (CR1).

**STEP2.** The cutting rate is reduced to CR2, as the new value of the compressive stress is the Eσ_{xx} for CR2 (Eσ_{xx} (CR2) = σ_{xx1}). The cut proceeds from Z1 to Z2, while the compressive stress reached the value σ_{xx2}, which is the Sσ_{xx} for CR = CR2.

**STEP3.** The cutting rate is further reduced to CR3, as the new value of the compressive stress (σ_{xx2}) is the Eσ_{xx} for CR3 (Eσ_{xx} (CR3) = σ_{xx2}). The cut proceeds up to the end (Z = Z3) with CR = CR3.
4.2 Correlations and Comprehensive Results Link

The experimental research hereby discussed allowed the estimation of the Sustainability limit stress $S_{\sigma_{zz}}$ for the compressed samples and the Efficiency limit stress $E_{\sigma_{zz}}$ for the tense samples. The comprehensive experimental plan is reported in Table 10, with the values of $CR^*$ and the correspondent limit values of $E_{\sigma_{zz}}$ and $S_{\sigma_{zz}}$. For the three generation pressures under investigation, Fig. 12 shows the interpolating curves of the experimental results, which clearly highlight the influence of the state of stress on the cutting rate: in compressed rocks, the increase of the absolute value of $\sigma_{zz}$ determines a reduction of the maximum $CR$; in tense rocks, the increase of the absolute value of $\sigma_{zz}$ determines an increase of the maximum $CR$. According to the cutting test, the $CR$ obtainable in unloaded samples of granite (0.63 m$^2$/h) is halved (0.30 m$^2$/h) when the compressive stress increases up to $-26.8$ MPa and becomes 1 m$^2$/h when the tensile stress reaches $+8$ MPa.

The mean slope of the interpolating curves ($\Delta CR/\Delta \sigma_{zz}$) in Fig. 12 also proves that the influence of the state of stress on CR is less relevant the greater the energy of the jet (higher generation pressure) and becomes negligible with generation pressure of 200 MPa. Table 11 reports the value of the mean slope $\Delta CR/\Delta \sigma_{zz}$ for each generation pressure in the experimental plan.

The results confirm the general relationship between $CR$ and the state of stress, which has already been discussed in previous studies, as well as the role of the generation.
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Table 10 Comprehensive experimental plan and results of test and numerical analysis – $p = 100$ MPa

| Test sample | Cutting rate (CR*) $(m^2/h)$ | Measured limit depth (mm) | Model | Lateral load (kN) | Simulated limit condition (depth of groove (mm)) | SubModel | $S_{\sigma_{xx}}$ (-) | $E_{\sigma_{xx}}$ (+) (MPa) |
|-------------|-----------------------------|---------------------------|-------|------------------|-----------------------------------------------|----------|---------------------|-------------------------|
| C1, a, b, c | 0.45 25 CM1 250 25 CM1α − 11.6 | 0.36 35 CM1 250 35 CM1β − 15.0 | 0.30 60 CM1 60 CM1χ − 26.8 |
| C2, a, b, c | 0.45 8 CM2 500 8 CM2α − 12.6 | 0.36 15 CM2 500 15 CM2β − 15.4 | 0.45 25 CM2 25 CM2χ − 22.4 |
| C1 a', b', c' | 1.30 23 CM1' 250 23 CM1α' − 11.0 | 1.1 61 CM1 61 CM1β' − 28.0 | |
| C2 a', b', c' | 0.90 44 CM2' 500 44 CM2α' − 44.5 | 0.83 64 CM2 64 CM2β' − 63.0 | |
| C1 a'', b'', c'' | 1.79 40 CM1' 250 40 CM1α'' − 18.0 | 1.78 65 CM1 65 CM1β'' − 32.0 | |
| C2 a'', b'', c'' | 1.75 65 CM2' 500 65 CM2α'' − 65.0 | 1.65 82 CM2 82 CM2β'' − 80.0 | |
| T1, a, b, c | 0.69 5 TM1 50 5 TM1α + 2.5 | 0.73 30 TM1 30 TM1β + 3.2 | |
| T2, a, b, c | 0.84 30 TM2 100 30 TM2α + 6.4 | 1.00 50 TM2 50 TM2β + 8.0 | |

Fig. 12 Comprehensive results and interpolating curves for the three values of the generation pressure
workable: the step function $\sigma_{xx}$–CR and effect of the water jet energy); nonetheless, the condition under exam: type of rock, cutting technology and operating parameters.

| Generation pressure (MPa) | $\Delta C/R / \Delta \sigma_{xx}$ (m$^2$/h)/MPa |
|--------------------------|------------------------------------------|
| 200                      | -1.1E3                                   |
| 160                      | -8.4E3                                   |
| 100                      | -1.4E2                                   |

Table 11 Mean slope of the interpolating curves $\sigma_{xx}$–CR$^*$ in Fig. 10

5 Conclusions

To assess the effect of the state of stress on the cutting rate CR, laboratory tests were performed with an oscillating water jet machine on granite samples of Rosa beta subjected to a static load. The stress distribution in the layer of rock to be removed was modeled with the FLAC code. The results confirmed that the increase of the state of stress due to the slot’s advancement causes the reduction of the maximum cutting rate in compressed rocks and the increase in rocks subjected to tensile stress.

Starting from a conceptual model, which theoretically explains the relationship between CR and the stress component $\sigma_{xx}$, a step function was defined that indicates the ranges $\Delta \sigma_{xx}$ where predefined values of the cutting rate (CR) are workable: the sustainability limit stress $\sigma_{xx}$ and the efficiency limit stress $\sigma_{xx}$ are the limits of those ranges. The sustainability limit stress was found for the granite samples subjected to compressive stress and the efficiency limit stress for those subjected to tensile stress. The test also proved the influence of the state of stress on the water jet cutting performance to be less relevant the greater the energy of the jet (higher generation pressure).

The implications of the research hereby discussed become apparent when considering the industrial implementation of the water jet technology to the extraction of granite in underground environments. In fact, the knowledge of the $\sigma_{xx}$–CR relationship allows planning the cutting sequence, so that the development of the state of stress within the rock massif is that which maximizes the average speed of the entire operation (i.e., minimizes the time required to isolate commercial blocks).

It should be noted that the overall outcome of the study has a general conceptual value (i.e., influence of $\sigma_{xx}$ on CR and effect of the water jet energy); nonetheless, the industrial application requires the experimental definition of the step function $\sigma_{xx}$–CR$^*$ for the specific operating condition under exam: type of rock, cutting technology and operating parameters.

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Declarations

Conflict of interest The authors declare that they have no conflicts of interest.

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