High-energy Neutrinos and Gamma Rays from Nonrelativistic Shock-powered Transients

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Abstract

Shock interaction has been argued to play a role in powering a range of optical transients, including supernovae, classical novae, stellar mergers, tidal disruption events, and fast blue optical transients. These same shocks can accelerate relativistic ions, generating high-energy neutrino and gamma-ray emission via hadronic pion production. The recent discovery of time-correlated optical and gamma-ray emission in classical novae has revealed the important role of radiative shocks in powering these events, enabling an unprecedented view of the properties of ion acceleration, including its efficiency and energy spectrum, under similar physical conditions to shocks in extragalactic transients. Here we introduce a model for connecting the radiated optical fluence of nonrelativistic transients to their maximal neutrino and gamma-ray fluence. We apply this technique to a wide range of extragalactic transient classes in order to place limits on their contributions to the cosmological high-energy gamma-ray and neutrino backgrounds. Based on a simple model for diffusive shock acceleration at radiative shocks, calibrated to novae, we demonstrate that several of the most luminous transients can accelerate protons up to $10^{16}$ eV, sufficient to contribute to the IceCube astrophysical background. Furthermore, several of the considered sources—particularly hydrogen-poor supernovae—may serve as “gamma-ray-hidden” neutrino sources owing to the high gamma-ray opacity of their ejecta, evading constraints imposed by the nonblazar Fermi Large Area Telescope background. However, adopting an ion acceleration efficiency of $\sim 0.3\%–1\%$ motivated by nova observations, we find that currently known classes of nonrelativistic, potentially shock-powered transients contribute at most a few percent of the total IceCube background.

Unified Astronomy Thesaurus concepts: Gamma-rays (637); Novae (1127); Supernovae (1668); Neutrino astronomy (1100)

1. Introduction

Optical time-domain surveys have in recent years discovered new classes of explosive transients characterized by a wide diversity of properties (e.g., Villar et al. 2017). These include exotic channels of massive-star death, such as “superluminous supernovae” (SLSNe; Gal-Yam 2019; Inserra 2019) of both hydrogen-rich (Smith et al. 2007) and hydrogen-poor (Quimby et al. 2011) varieties; tidal disruption events (TDEs) of stars by massive black holes (Gezari et al. 2012; Stone et al. 2019); “luminous red novae” (LRNe; e.g., Tylenda et al. 2011) and dusty infrared-bright transients (Kasliwal et al. 2017) from merging binary stars; and “fast blue optical transients” (FBOTs; e.g., Drout et al. 2014) of an uncertain origin likely related to massive-star death.

Many of these events reach peak luminosities that are greater than can be understood by the traditional energy sources available to SNe, such as radioactive decay or the initial heat generated during the dynamical explosion, merger, or disruption. An additional, internal power source is clearly at play. One of the most promising ways of enhancing the optical output from a transient is via shocks, generated as the explosion ejecta (or streams of stellar debris in the case of TDEs) collide with themselves or an external medium. For a wide range of conditions these shocks are radiative, meaning that, due to the high gas densities, the thermal cooling time behind the shock is short compared to the expansion time. Under these conditions, the shocked gas emits copious UV/X-ray emission, which is absorbed with high efficiency by surrounding gas and “reprocessed” downward into the visual wave band, enhancing or even dominating the transient light (e.g., Chevalier & Fransson 1994).

Shock interaction is commonly invoked to power the light curves of SLSNe (e.g., Smith & McCray 2007; Chevalier & Irwin 2011; Moriya et al. 2014; Sorokina et al. 2016), particularly the hydrogen-rich variety (SLSNe II), in which narrow emission lines directly reveal the presence of dense slow gas ahead of the ejecta (dubbed “Type IIn” when the hydrogen lines are narrow; Schlegel 1990). However, embedded shock interaction could also power SN light curves even in cases where emission features or other shock signatures are not visible, for example, when a compact circumstellar disk is overtaken by faster opaque ejecta (e.g., Andrews & Smith 2018). Shells or outflows of dense external gas surrounding SNe can be the result of intense mass loss from the star in the years and decades prior to its explosion (Smith 2014). In the case of extremely massive, metal-poor stars, this can include impulsive mass ejection as a result of the pulsational pair instability (Woosley et al. 2007; Tolstov et al. 2016).

Similarly in binary star mergers, shock interaction can take place between fast matter ejected during the dynamical “plunge” phase at the end of the merger process and slower outflows from the earlier gradual inspiral (Pejcha et al. 2017;
MacLeod et al. 2018); these embedded shocks may be responsible for powering the plateau or secondary maxima observed in the light curves of LRNe (Metzger & Pejcha 2017). Shock-mediated collisions between the bound streams of the disrupted star in TDEs may power at least part of the optical emission in these events (Piran et al. 2015; Jiang et al. 2016).

The optical emission from FBOTs, such as the nearby and well-studied AT2018cow (Prentice et al. 2018; Perley et al. 2019), could also be powered by internal shock interaction in explosions with a low ejecta mass (Margutti et al. 2019; Tolstov et al. 2019; Piro & Lu 2020).7

In each of the extragalactic transients cited above, the inference of shock interaction is at best indirect. However, a direct confirmation of embedded shock-powered emission has become possible recently from a less energetic (but comparatively nearby) class of Galactic transients: the classical novae. Over the past decade, the Fermi Large Area Telescope (LAT) has detected \( \sim 0.1–10 \) GeV gamma-ray emission coincident with the optical emission from over 10 classical novae (Ackermann et al. 2014; Cheung et al. 2016; Franckowiak et al. 2018). The nonthermal gamma rays are generated by relativistic particles accelerated at shocks (via the diffusive acceleration process; Blandford & Ostriker 1978; Eichler 1979; Bell 2004), which arise owing to collisions internal to the nova ejecta (Chomiuk et al. 2014; Metzger et al. 2014a).

Nonthermal gamma-ray emission in novae could in principle be generated either by relativistic electrons (which Compton-uncat the nova optical light or emit bremsstrahlung radiation in the GeV band)—the “lepton” mechanism—or via relativistic ions colliding with ambient gas (generating pions that decay into gamma rays—the “hadronic” mechanism). However, several arguments favor the hadronic mechanism and hence the presence of ion acceleration at nova shocks. For example, strong magnetic fields are required near the shocks to confine and accelerate particles up to sufficiently high energies \( \gtrsim 10–100 \) GeV to generate the observed gamma-ray emission; embedded in the same magnetic field, however, relativistic electrons lose energy to lower-frequency synchrotron radiation faster than it can be emitted as gamma rays, disfavoring the leptonic models (Li et al. 2017; Vurm & Metzger 2018).

The ejecta surrounding the shocks in novae are sufficiently dense to act as a “calorimeter” for converting nonthermal particle energy into gamma rays (Metzger et al. 2015). For similar reasons of high densities, the shocks are radiative and their power is reprocessed into optical radiation with near-unity efficiency (Metzger et al. 2014a). Stated another way, both the thermal and nonthermal particles energized at the shocks find themselves in a fast-cooling regime. As a result, the gamma-ray and shock-powered optical emission should trace one another, and the ratio of their luminosities can be used to directly probe the particle acceleration efficiency (Metzger et al. 2015). In two novae with high-quality gamma-ray light curves, ASASSN 16ma (Li et al. 2017) and V906 Car (Aydi et al. 2020), the time-variable optical and gamma-ray light curves are observed to track each other, confirming predictions that radiative shocks can power the optical emission in novae (Metzger et al. 2014a).

Applying the above technique, one infers an efficiency of nonthermal particle acceleration in novae of \( \epsilon_{\text{rel}} \sim 0.3\%–1\% \) (Li et al. 2017; Aydi et al. 2020). This is low compared to the \( \epsilon_{\text{rel}} \sim 10\% \) efficiency one finds for the adiabatic shocks in SN remnants (e.g., Morlino & Caprioli 2012) or the maximal value \( \epsilon_{\text{rel}} \sim 20\% \) found from particle-in-cell simulations of diffusive shock acceleration for the optimal case in which the upstream magnetic field is quasi-parallel to the shock normal (Caprioli & Spitkovsky 2014a). In novae—as in other shock-powered transients—the magnetic field of the upstream medium is generally expected to be wrapped in the toroidal direction around the rotation axis of the outflow (“Parker spiral”; Parker 1958), perpendicular to the radial shock direction and hence in the quasi-perpendicular regime for which little or no particle acceleration is theoretically predicted (Caprioli & Spitkovsky 2014a). The small efficiency \( \sim 0.3\%–1\% \) that nevertheless is obtained may arise owing to the irregular, corrugated shape of the radiative-shock front, which allows local patches of the shock to possess a quasi-parallel shock orientation and hence to efficiently accelerate particles (Steinberg & Metzger 2018).

Gamma rays generated from the decay of \( \pi^0 \) in hadronic accelerators are accompanied by a similar flux of neutrinos from \( \pi^- \) decay. A future detection of \( \sim \) GeV–TeV neutrino emission, likely from a particularly nearby nova, would thus serve as a final confirmation of the hadronic scenario (Razzaque et al. 2010; Metzger et al. 2016). However, compared to SNe, the relatively low kinetic energies of classical novae make them subdominant contributors to the cosmic-ray or neutrino energy budget in the Milky Way or other galaxies. On the other hand, with the exception of their luminosities, many of the physical conditions that characterize nova shocks (gas density, evolution timescale) are broadly similar to those of more energetic extragalactic transients. The advantage of novae—being among the brightest transients in the night sky—is their relative proximity, which enables a detailed view of their gamma-ray emission and hence particle acceleration properties.

For comparison, nonthermal gamma rays have not yet been detected from extragalactic SNe in either individual or stacked analysis (Ackermann et al. 2015b; Renault-Tinacci et al. 2018; Murase et al. 2019), with a few possible exceptions (Yuan et al. 2018; Xi et al. 2020). This is despite the potential for shock interaction within these sources—if prevalent—to be major contributors of high-energy cosmic rays, gamma rays, and neutrinos (e.g., Chakraborti et al. 2011; Katz et al. 2011; Murase et al. 2011, 2014; Kashiyama et al. 2013; Zirakashvili & Ptuskin 2016; Marcowith et al. 2018; Murase 2018; Zhang & Murase 2019; Cristofari et al. 2020).

In this paper we apply the knowledge of particle acceleration at radiative shocks, as gleaned from recent studies of classical novae (Li et al. 2017; Aydi et al. 2020), to assess the prospects of interacting SNe and other nonrelativistic, shock-powered extragalactic transients as sources of high-energy gamma-ray emission and neutrinos. An astrophysical neutrino population above \( \sim 10 \) TeV has been measured by the IceCube Observatory (IceCube Collaboration et al. 2013; Schneider 2019; Stettner 2019). The sources that contribute to the bulk of high-energy neutrinos remain unknown (IceCube Collaboration et al. 2020a, 2020b), though hints of sources have been suggested (Aartsen et al. 2018; IceCube Collaboration et al. 2018, 2020b). We are thus motivated to consider to what extent

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7 However, note that an energetic compact object—a newly born magnetar or accreting black hole—provides an alternative energy source in FBOTs and SLSNe (Kasen & Bildsten 2010; Woosley 2010), which could also be a source of neutrinos (Fang et al. 2019).
shock-powered transients, under optimistic but realistic (i.e., observationally calibrated) assumptions, are capable of contributing to the neutrino background.

Intriguingly, the magnitude of IceCube’s diffuse neutrino flux is comparable to that of the Fermi LAT isotropic γ-ray background (IGRB) around $\sim 100$ GeV (Ackermann et al. 2015a; Di Mauro & Donato 2015), and to avoid overestimating the IGRB, the neutrino sources were suggested to be “hidden,” i.e., locally opaque to 1–100 GeV γ-rays (e.g., Berezhný & Dokuchaev 2001; Murase et al. 2016; Capanema et al. 2020a, 2020b). Given the high column densities of shock-powered transients, they offer one of only a handful of potentially gamma-ray-hidden neutrino sources, further motivating our study.

This paper is organized as follows. In Section 2 we introduce a simple model for nonrelativistic shock-powered transients and describe the connection between their high-energy gamma-ray/neutrino and optical emissions, as probed via the calorimetric technique. In Section 3 we apply the methodology to classical novae and show how observations (particularly modeling of their gamma-ray spectra) can be used to calibrate uncertain aspects of the acceleration process in radiative shocks. In Section 4 we apply the calorimetric technique to place upper limits on the high-energy neutrino and gamma-ray background from the “zoo” of (potentially) shock-powered transients across cosmic time and compare them to constraints from IceCube and Fermi. In Section 5 we summarize our conclusions.

2. Shock-powered Supernovae as Cosmic-Ray Calorimeters

This section introduces a simplified, but also fairly generic, model of shock-powered transients and the general methodology for using their optical light curves to constrain their high-energy gamma-ray and neutrino emission (see Figure 1 for a schematic illustration). In places where specificity is necessary, we focus on the particular case of interaction-powered SNe. However, most of the conditions derived are broadly applicable to any transient (e.g., novae, TDEs, stellar mergers) in which a nonrelativistic shock is emerging from high to low optical depths. Insofar as possible, we express our results exclusively in terms of observable quantities such as the optical rise time, peak luminosity, or characteristic expansion velocity (measurable, e.g., from optical spectroscopy).

2.1. Shock Dynamics and Thermal Emission

We consider the collision of spherically expanding homologous ejecta of average velocity $v_{ej}$ generated during a dynamical explosion with an effectively stationary external medium (the treatment can easily be generalized to a moving upstream or aspherical ejecta, but for nonrelativistic expansion this generally introduces only order-unity changes). The external medium is assumed to possess a nucleon number density $n \equiv \rho/m_p$ (where $\rho$ is the mass density) with a radial profile $n \propto r^{-k}$, where $k \geq 2$ is a power-law index, and to be concentrated into a fractional solid angle $f_{\Omega} \leq 1$ (e.g., $f_{\Omega} \approx h/r$ if the external medium is concentrated in a thin equatorial disk of vertical scale height $h$ and aspect ratio $h/r$).

One convenient parameterization of the density profile is that of a steady wind of mass-loss rate $M$ and velocity $v_w$ such that $n \approx M/(4\pi f_{\Omega} r^2 v_w^2 m_p) \equiv A/(m_p r^2)$, where $A \equiv M/(4\pi f_{\Omega} v_w)$. For example, values of $M \sim 10^{-4} - 1 M_\odot\ yr^{-1}$ and $v_w \sim 100 - 1000\ km\ s^{-1}$ are typically inferred by modeling interacting SNe (e.g., Smith 2014), corresponding to $A \approx 1 - 10^4 A_f$, where $A_f \equiv 5 \times 10^{11}\ g\ cm^{-2}$ is a fiducial value for $M = 10^{-3} M_\odot\ yr^{-1}$ and $v_w = 1000\ km\ s^{-1}$ (Chevalier & Li 2000). In general, we expect $k \geq 2$ if the value of $M$ is increasing approaching the explosion or dynamical event, as may characterize wave-driven mass loss from massive stars before they explode as SNe (e.g., Quataert & Shiode 2012) or binary star mergers in which the merger is instigated by unstable mass transfer and mass loss that arises rapidly approaching the dynamical coalescence phase (e.g., Pejcha et al. 2017). In such cases where $k > 2$ the effective value of $A(r)$ is a (decreasing) function of radius, though this detail is not important, as we are primarily interested in its value near the optical peak, as discussed further below.

The collision drives a forward shock into the external medium and a reverse shock back into the ejecta. When the shocks are radiative (the conditions for which will be verified below), the gas behind both shocks rapidly cools and accumulates into a thin central shell, which propagates outward into the external medium at a velocity $v_{sh}$ equal to that of the forward shock. The shocks reach a radius $R_{sh} \approx v_{sh} t$ by a time $t$ after the explosion. Given the homologous velocity profile of the ejecta (inner layers slower than outer layers; $v_{ej} \propto r$), in many cases of interest the shell is accelerated to a velocity matching that of the ejecta at a similar radius (e.g., Metzger & Pejcha 2017), reducing the power of the reverse shock relative to the forward shock by the times of interest near the light-curve peak. Although the discussion to follow focuses on the forward-shock-dominated case for concreteness, qualitatively similar results apply to the reverse-shock-dominated case.

The kinetic power of the forward shock is given by

$$L_{sh} = \frac{9}{8} f_{\Omega} m_p n_{sh} v_{sh}^3 R_{sh}^2 = \frac{9}{32} M_{sh}^3 v_w = \frac{9}{8} A_f v_{sh}^3,$$

(1)

where $n_{sh} \equiv n(R_{sh})$ is the characteristic upstream density ahead of the shock and $f_{\Omega} \leq 1$ is again the fractional solid angle subtended by the shocks’ interaction (Figure 1). Gas immediately behind the shock is heated to a temperature

$$k T_{sh} \approx \frac{3}{16} \mu m_p v_{sh}^2 \approx 11 v_{sh}^2\ km\ s^{-1},$$

(2)

where $v_{sh} \approx v_w/(3000\ km\ s^{-1})$ and we have taken $\mu = 0.62$ for the mean molecular weight of fully ionized gas of solar composition (we would instead have $\mu \approx 2$ if the upstream medium is composed of hydrogen-poor gas). The bulk of the shock’s power $\sim L_{sh}$ is emitted at temperatures $\sim k T_{sh}$ (in the X-ray range for typical shock velocities $v_{sh} \gtrsim 10^3\ km\ s^{-1}$). However, due to the large photoelectric opacity of the external medium (at the times during peak light when the bulk of the particle acceleration occurs; see below), most of $L_{sh}$ is absorbed and reprocessed via continuum and line emission into optical wavelengths (consistent, e.g., with the nondetection of luminous X-rays from SLSNe near optical peak; Levan et al. 2013; Ross & Dwarkadas 2017; Margutti et al. 2018).

The shock luminosity $L_{sh}$ is only available to contribute to the SN light curve after a certain time. To escape to an external observer, reprocessed emission from the vicinity of the forward shock must propagate through the column of the external

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shock-powered optically radiated energy. The thickness of the postshock region as set by thermal cooling, the maximum particle energy achievable via diffusive shock acceleration X-ray emission from the thin cooling layer behind the shocks is absorbed and reprocessed by the surrounding gas into optical radiation of luminosity fractional solid angle required for the formation of a collisionless shock capable of particle acceleration. At this epoch of peak emission, both thermal particles emission light curve peaks, and the bulk of particle acceleration occurs, when the optical depth surrounding the shock first obeys the condition \( \tau_{\text{opt}} \lesssim c / v_{\text{sh}} \) similar to that required for the formation of a collisionless shock capable of particle acceleration. At this epoch of peak emission, both thermal particles (which emit via free–free emission) and nonthermal particles (undergoing p–p interactions) are radiative, such that the emitted nonthermal gamma-ray/neutrino emission is proportional to the shock-powered optically radiated energy. The thickness of the postshock region as set by thermal cooling, \( \Delta R_{\text{cool}} \), is much smaller than the shock radius \( R_{\text{sh}} \), limiting the maximum particle energy achievable via diffusive shock acceleration (Equation (16)).

The explosion ejecta collides with a dense external medium (e.g., circumstellar medium, CSM) of radial density profile \( n(r) \) and effective wind mass-loss rate parameter \( \Lambda \equiv M / (4 \pi c v_w) \), which covers a fractional solid angle \( f_0 < 1 \). The ejecta of mean velocity \( v_e \) collides with the CSM, driving a shock into the latter with a velocity \( v_{\text{sh}} \) and kinetic luminosity \( L_{\text{sh}} \). UV/X-ray emission from the thin cooling layer behind the shocks is absorbed and reprocessed by the surrounding gas into optical radiation of luminosity \( L_{\text{opt}} \approx L_{\text{sh}} \). The shock also accelerates relativistic ions that collide with background ions, generating \( \pi^+ \) and \( \pi^- \), which decay into gamma rays and neutrinos, respectively. The optical light curve peaks, and the bulk of particle acceleration occurs, when the optical depth surrounding the shock first obeys the condition \( \tau_{\text{opt}} \lesssim c / v_{\text{sh}} \), similar to that required for the formation of a collisionless shock capable of particle acceleration. At this epoch of peak emission, both thermal particles (which emit via free–free emission) and nonthermal particles (undergoing p–p interactions) are radiative, such that the emitted nonthermal gamma-ray/neutrino emission is proportional to the shock-powered optically radiated energy. The thickness of the postshock region as set by thermal cooling, \( \Delta R_{\text{cool}} \), is much smaller than the shock radius \( R_{\text{sh}} \), limiting the maximum particle energy achievable via diffusive shock acceleration (Equation (16)).

Medium, \( \Sigma = \int_{R_{\text{sh}}}^{\infty} n dr \sim n_{\text{sh}} R_{\text{sh}} \). The reprocessed optical light will emerge without experiencing adiabatic losses provided that the optical photon diffusion timescale \( t_{\text{diff}} \approx \tau_{\text{opt}} \left( R_{\text{sh}} / c \right) \), where \( \tau_{\text{opt}} \equiv \Sigma \sigma_{\text{opt}} \), with \( \sigma_{\text{opt}} \) the effective cross section at visual wavelengths, is shorter than the expansion timescale of the shocked gas, \( t_{\text{dyn}} \sim R_{\text{sh}} / v_{\text{sh}} \), over which adiabatic losses occur, i.e.,

\[
\tau_{\text{opt}} \lesssim c / v_{\text{sh}},
\]

as is satisfied at times

\[
t \gtrsim t_{\text{pk}} \approx \frac{c}{v_{\text{sh}} n_{\text{sh}} \sigma_{\text{opt}}} = \frac{M \kappa_{\text{opt}}}{4 \pi f_{\Omega} c v_w} = \frac{A \kappa_{\text{opt}}}{c},
\]

where \( \kappa_{\text{opt}} \equiv \sigma_{\text{opt}} / m_e \) is the optical opacity. We label this critical time \( t_{\text{pk}} \) since it defines the rise time, and often the peak timescale, of the light curve.

Equation (4) neglects corrections to \( t_{\text{diff}} \) due to nonspherical geometry and assumes that the diffusion of reprocessed optical photons outward through the shocked gas is the rate-limiting step to their escape, as opposed to additional diffusion through the surrounding ejecta. Although this assumption is justified in many cases, it is clearly violated in certain cases (e.g., highly aspherical ejecta, \( f_0 \ll 1 \); very low CSM mass relative to ejecta mass). Nevertheless, our cavalier approach is justified since the main goal of our analysis is to provide order-of-magnitude estimates of the shock properties near optical maximum.

For a wide range of shock-dominated transients, \( t_{\text{pk}} \) sets the rise time of the light curve to its peak luminosity \( L_{\text{pk}} \approx L_{\text{sh}} = (9 \pi / 8) A_{f_{\Omega}} v_{\text{sh}}^2 \) (Equation (1)), with \( L_{\text{opt}} \ll L_{\text{sh}} \) at times \( t \ll t_{\text{pk}} \) and \( L_{\text{opt}} \approx L_{\text{sh}} \) at \( t \gtrsim t_{\text{pk}} \). In general, \( L_{\text{sh}} \) (and hence \( L_{\text{opt}} \)) will decrease after \( t_{\text{pk}} \) because \( A(r) \) is decreasing with radius or because \( v_{\text{sh}} \) is decreasing as the shock sweeps up mass.

Combining Equations (1) and (4), we can express the shock velocity,

\[
v_{\text{sh}} = \left( \frac{8}{9 \pi c t_{\text{pk}} f_{\Omega}} \right)^{1/3} L_{\text{pk}} \kappa_{\text{opt}},
\]

in terms of the two other “observables,” \( L_{\text{pk}} \) and \( t_{\text{pk}} \). Here we have assumed that 100% of the transient’s optical light is shock powered, \( L_{\text{pk}} \approx L_{\text{sh}}(t_{\text{pk}}) \), i.e., neglecting additional contributions to \( L_{\text{pk}} \) from, e.g., radioactivity, initial thermal energy, or a central engine (though the latter can be a source of energizing
the ejecta and driving shocks; e.g., Metzger et al. 2014b; Kasen et al. 2016; Fang & Metzger 2017; Decoene et al. 2020).

2.2. The Calorimetric Technique

Remarkably, conditions (3) and (4) on the optical depth to the shock are very similar to that required for the shock discontinuity to be mediated by collisionless plasma processes instead of by radiation (e.g., Colgate 1974; Klein & Chevalier 1978; Katz et al. 2011). Before this point when the optical depth is higher, relativistic-particle acceleration is not possible because trapped radiation thickens the shock transition to a macroscopic scale, precluding the particle injection process (Zel’dovich & Raizer 1967; Weaver 1976; Riffert 1988; Lyubarskii & Syunyaev 1982; Katz et al. 2011; Waxman & Katz 2017).

This has two implications: (1) efficient relativistic-particle acceleration is unlikely to occur in interacting SNe and other shock-powered transients well prior to the optical peak, and (2) if a fixed fraction \( \epsilon_{\text{rel}} \) of the shock power \( L_{\text{sh}} \) is placed into relativistic particles (once Equation (3) is satisfied), the total energy placed into relativistic particles \( (E_{\text{rel}} \approx \int_{t_{\text{sh}}}^{t_{\text{pk}}} \epsilon_{\text{rel}} L_{\text{sh}} dt) \) is proportional to the fraction, \( f_{\text{sh}} \), of the radiated optical fluence of the SN \( (E_{\text{opt}} \approx f_{\text{sh}}^{-1} \int_{t_{\text{pk}}}^{\infty} L_{\text{sh}} dt) \) that is powered by shocks. In other words,

\[ E_{\text{rel}} \approx f_{\text{sh}} \epsilon_{\text{rel}} E_{\text{opt}}. \tag{6} \]

As a corollary, since \( f_{\text{sh}} < 1 \), this implies that \( \epsilon_{\text{rel}} E_{\text{opt}} \) is an upper limit on the energy of accelerated relativistic particles. Insofar as the relativistic particles are fast cooling and will generate gamma rays/neutrinos in direct proportion to \( E_{\text{rel}} \) (the calorimetric limit; Metzger et al. 2015), this in turn implies that the total optical energy of all shock-powered transients in the universe places an upper bound on the gamma-ray/neutrino background given some assumption about the value of \( \epsilon_{\text{rel}} \) and the spectrum of nonthermal particles (in our case motivated by observations of novae). This is the main technique applied in this paper.

Before proceeding, we must prove several assumptions made above, using \( t \sim t_{\text{pk}} \) (Equation (4)) as the critical epoch at which we must check their validity. First, consider the assumption that the shocks are radiative. Thermal gas behind the shock will cool radiatively on a timescale

\[ t_{\text{cool}} = \frac{\mu c}{\mu_p} \frac{3 k T_{\text{sh}}}{8 \Lambda n_{\text{sh}}} = \frac{9 m_p v_{\text{sh}}^2}{128 \Lambda n_{\text{sh}}}, \tag{7} \]

where \( \Lambda \) is the cooling function at \( T = T_{\text{sh}} \) and we have evaluated \( T_{\text{sh}} \) using Equation (2). Here \( \mu_c = 2/(1 + X) \approx 1.16 \) and \( \mu_p = 1/X \approx 1.39 \) for hydrogen mass fraction \( X = 0.72 \). At high temperatures \( T \gtrsim 10^{7.3} \text{K} \) free–free cooling dominates, for which \( \Lambda \approx \Lambda_{\text{ff}} \approx 2.3 \times 10^{-27} (T_{\text{sh}}/K)^{1/2} \text{erg cm}^2 \text{s}^{-1} \) (Draine 2011).8 The ratio of cooling to the shock dynamical timescale is thus

\[ \frac{t_{\text{cool}}}{t_{\text{dyn}}} \bigg|_{\text{ff}} = \frac{9 \kappa_{\text{opt}} m_p v_{\text{sh}}^4}{128 c \Lambda} \approx 10^{-3} \kappa_{\text{opt}} v_{\text{sh}}^{-3}, \tag{8} \]

where we have normalized \( \kappa_{\text{opt}} = 0.3 \kappa_{0.3} \text{cm}^2 \text{g}^{-1} \) to a characteristic optical opacity similar to the electron scattering

8 At lower temperatures, \( 10^3 < T < 10^7 \text{K} \), cooling from line emission also contributes, with \( \Lambda_{\text{line}} \approx 1.1 \times 10^{-76} (T_{\text{sh}}/\text{K})^{-1/2} \text{erg cm}^2 \text{s}^{-1} \) (Draine 2011).

value for fully ionized gas \( \kappa_{\text{opt}} \approx \sigma_T/m_p \approx 0.38 \text{cm}^2 \text{g}^{-1} \), a reasonable approximation for hydrogen-rich ejecta; however, the opacity may be somewhat lower owing to lower ionization in the case of hydrogen-poor SNe (e.g., SLSNe I), where it may instead result from Doppler-broadened Fe lines (e.g., Pinto & Eastman 2000). From Equation (8) we conclude that the shocks are generically radiative \( (t_{\text{cool}} \ll t_{\text{dyn}}) \) at the epoch of peak light/relativistic-particle acceleration, for shock velocities \( v_{\text{sh}} \lesssim 10,000–30,000 \text{km} \text{s}^{-1} \), which agrees with the findings of Murase et al. (2011), Kashiyama et al. (2013), and Murase et al. (2014).

What about the nonthermal particles? Relativistic ions accelerated at the shock (when it becomes collisionless at times \( t > t_{\text{pk}} \)) will carry a power given by \( L_{\text{rel}} \approx \epsilon_{\text{rel}} L_{\text{sh}} \) and a total energy \( E_{\text{rel}} \) (Equation (6)), where \( \epsilon_{\text{rel}} \sim 0.003–0.01 \) in novae (Section 3). After escaping the shock upstream into the unshocked ejecta, or being advected downstream into the cold shell, the relativistic ions will undergo inelastic collisions with ambient ions, producing pions and their associated gamma-ray and neutrino emission.9 This interaction occurs on a timescale \( t_{\text{pp}} \approx (t_{\text{opt}})^{-1} \), where \( t_{\text{opt}} \approx 5 \times 10^{-26} \text{cm}^3 \text{s}^{-1} \) is the inelastic proton–proton cross section around 1 PeV (Particle Data Group 2020). Again, considering the ratio

\[ \frac{t_{\text{pp}}}{t_{\text{dyn}}} = \frac{\left( \frac{v_{\text{sh}}}{c} \right)^5}{\frac{\sigma_{\text{pp}}}{\sigma_{\text{opt}}}} \approx 10^{-3} \kappa_{0.3} v_{\text{sh}}^{-3}, \tag{9} \]

we see that \( t_{\text{pp}} \ll t_{\text{dyn}} \) for \( v_{\text{sh}} \gtrsim 30,000 \text{km} \text{s}^{-1} \). As in the case of thermal particles, relativistic particles (above the threshold energy) will pion-produce on a timescale much shorter than they would lose their acquired energy to adiabatic expansion of the ejecta.10

Protons may also interact with the ambient photons through photopion production when their energy is above the pion production threshold, \( E_{p,\text{th}} \approx (\epsilon_{p,\text{th}}/\epsilon_{\text{opt}}) m_p c^2 = 1.4 \times 10^{16} (\epsilon_{\text{opt}}/10 \text{eV})^{-1} \text{eV} \), with \( \epsilon_{p,\text{th}} \approx (m_e + m_p^2/m_p)c^2 \approx 150 \text{MeV} \). When the photopion production is allowed, it may play an important role with a competing timescale compared to the \( p-p \) interaction,

\[ \frac{t_{\text{pp}}}{t_{p\gamma}} = \frac{9}{32} \frac{m_p v_{\text{sh}}^2}{\epsilon_{\text{opt}}} \frac{\sigma_{p\gamma}}{\sigma_{\text{pp}}} \approx 4 v_{\text{sh}}^{-3} \epsilon_{\text{opt}}^{-1/2} f_{\text{sh}}, \tag{10} \]

where \( \sigma_{p\gamma} \approx 70 \mu \text{b} \) is the inelastic photopion interaction cross section (Dermer & Menon 2009). For most of the parameter space in consideration, the threshold energy can only be reached when \( f_{\text{sh}} \ll 1 \). We thus do not account for the neutrino production from the photopion production in the calculation below.

The charged pions created by \( p-p \) interactions may themselves interact with background protons, at a rate \( t_{p\gamma}^{-1} \approx (n \sigma_{p\gamma} c) \), or produce synchrotron radiation, at a rate \( t_{\gamma}^{-1} \approx 4 \sigma_T u_B c \gamma_{\text{sync}} (m_e/m_p)^2/3 m_e c^2) \). In the above expressions
\[ \sigma_{\text{np}} \approx 4 \times 10^{-26} \text{ cm}^2 \] is the inelastic pion–proton cross section around 0.1–1 PeV (Particle Data Group 2020), and \( u_B = B^2 / (8 \pi) \) is the magnetic field energy density, with \( B \) defined later in Equation (13). However, these interaction timescales,

\[ \frac{t_{\text{np}}}{\gamma_\pi \tau_\pi} \approx \frac{V_{\text{sh}}}{c} \left( \frac{\sigma_{\text{opt}}}{\sigma_{\text{np}}} \right) \left( \frac{t_{pk}}{\gamma_\pi \tau_\pi} \right) \approx 2 \times 10^5 \frac{\kappa_{\text{ion}}}{\kappa_{\text{opt}}} \frac{1}{\gamma_\pi \tau_\pi} t_{pk,\text{month}} \tag{11} \]

and

\[ \frac{t_{\text{p, syn}}}{\gamma_\pi \tau_\pi} \approx 9 \times 10^7 \frac{\gamma_\pi}{\epsilon_{Z}} \frac{1}{\kappa_{\pi,6}} t_{pk,\text{month}} \tag{12} \]

are much longer than the charged pion lifetime \( \gamma_\pi \tau_\pi \), where \( \tau_\pi = 2.6 \times 10^{-8} \text{ s} \) is the average lifetime of charged pions at rest and \( \gamma_\pi = 10^6 \gamma_{\pi,6} \) is a typical Lorentz factor. Similarly, one can show that around the peak time muons also quickly decay into neutrinos without much cooling.

Equations (8) and (9) show that both thermal and nonthermal particles cool effectively instantaneously at the epoch of peak shock power, thus forming the theoretical basis for using shock-powered transients as cosmic-ray calorimeters (Metzger et al. 2015).

### 2.3. Maximum Ion Energy

In the paradigm of diffusive shock acceleration, as cosmic rays gain greater and greater energy \( E \), they can diffuse back to the shock from a greater downstream distance because of their larger gyroradii \( r_\pi = E / (Z e B_{\text{sh}}) \), where \( B_{\text{sh}} \) is the strength of the turbulent magnetic field near the shock and \( Z e \) is the particle charge. A promising candidate for generating the former is the hybrid nonresonant cosmic-ray current-driven streaming instability (nonresonant hybrid; Bell 2004). The magnetic field strength near the shock may be estimated using equipartition arguments:

\[ B_{\text{sh}} = \left( 6 \pi \frac{e_B m_p n_{\text{sh}} V_{\text{sh}}^2}{\gamma_\pi} \right)^{1/2} \tag{13} \]

where \( e_B \ll 1 \) is the ratio of the magnetic energy density to the immediate postshock thermal pressure.

The maximum energy to which particles are accelerated before escaping the cycle, \( E_{\text{max}} \), is found by equating the upstream diffusion time \( t_{\text{diff}} \sim D / V_{\text{sh}}^2 \) with the downstream advection time \( t_{\text{adv}} \sim \Delta R_{\text{acc}} / V_{\text{sh}} \), where \( \Delta R_{\text{acc}} \) is the width of the acceleration zone. Taking \( D \approx r_\pi c / 3 \) as the diffusion coefficient (Caprioli & Spitkovsky 2014b), one obtains

\[ E_{\text{max}} \sim \frac{3eZB_{\text{sh}}V_{\text{sh}} \Delta R_{\text{acc}}}{c} \tag{14} \]

What is the appropriate value of \( \Delta R_{\text{acc}} \)? In the case of fully ionized, nonradiative (adiabatic) shocks, it may be justified to take \( \Delta R_{\text{acc}} \sim R_{\text{sh}} \), i.e., to assume that particle acceleration occurs across a large fraction of the system size. However, in shock-powered transients, the high gas densities result in very short radiative recombination times, rendering the gas far upstream or downstream of the shock quasi-neutral. Neutral gas is challenged to support a strong magnetic field, and ion-neutral damping can suppress the growth of the NRH (Reville et al. 2007). Indeed, in novae the temperature ahead of the shocks may in some cases be too low for efficient collisional ionization, in which case the radial extent of \( \Delta R_{\text{acc}} \) into the upstream flow is a narrow layer ahead of the shock that has been photoionized by the shock’s UV/X-ray emission (Metzger et al. 2016).

In luminous extragalactic transients with high effective temperatures near optical peak—the main focus of this paper—ionization is less of a concern than in novae. However, the maximal extent of the particle acceleration zone behind the shock is still limited because of thermal cooling, which compresses the length of the postshock region to a characteristic width \( \Delta R_{\text{cool}} \sim v_{\text{sh}} \tau_{\text{cool}} \), where \( t_{\text{cool}} \) is defined in Equation (7). Taking \( \Delta R_{\text{acc}} = \Delta R_{\text{cool}} \) in Equation (14), we obtain

\[ E_{\text{max}} \sim \frac{3eZB_{\text{sh}}V_{\text{sh}} t_{\text{cool}}}{c} \tag{15} \]

where in the second line we have used Equations (1) and (13). Evaluating this at \( t = t_{pk} \), we find

\[ E_{\text{max}} / m_p \approx 3 \times 10^{44} \text{ eV} \tag{16} \]

with \( \kappa_{\pi,2} \sim 0.3 \kappa_{\text{ion}} \), where \( \kappa_{\pi,2} \) is the cooling factor for \( \gamma_{\text{cool},43} \approx 1 \times 10^{44} \text{ erg s}^{-1} \), and we have evaluated Equation (8) for \( t_{\text{cool}} / t_{pk} \).

For a large shock velocity, the proton–proton interaction time may be shorter than the advection time across the cooling length \( t_{pp} < t_{cool} \). In this regime, the maximum energy is determined by \( t_{\text{diff}} \sim t_{pp} \) and we can obtain a similar form as in Equation (15),

\[ E_{\text{max}} \sim \frac{3eZB_{\text{sh}}V_{\text{sh}} t_{pp}}{c} \tag{17} \]

with \( t_{pp} / t_{pk} \) at the peak time evaluated in Equation (9).

Thus, \( E_{\text{max}} \) is a very sensitive function of the shock velocity. Since in most cases \( V_{\text{sh}} \) and \( L_{\text{sh}} \) will decrease as the shock sweeps up gas (and since nonthermal particle acceleration cannot occur at times \( t \ll t_{pk} \)), \( E_{\text{max}} / m_p \) is a reasonably good proxy for the maximum particle energy achieved over the entire shock interaction.

The inelastic collisions of ions of energy \( E \) with ambient ions to generate \( \Delta E \left( \pi^+ \right) \) will typically produce gamma rays (neutrinos) of energy \( \sim 0.1 E \) (0.05 E) (Kelner & Aharonian 2008). Given the characteristic values up to \( E_{\text{max}} \approx 10^{16} \text{ eV} \) implied by Equation (16) for characteristic velocities \( V_{\text{sh}} \sim V_{\text{sh},43} \approx 10,000 \text{ km s}^{-1} \) and luminosities \( L_{\text{sh}} \sim L_{\text{sh},43} \approx 10^{44} \text{ erg s}^{-1} \) of the most luminous astrophysical transients (e.g., TDEs and SLSNe) under the assumption that their light curves are shock powered, we see that high-energy photons and neutrinos ranging in energy from \( \sim 1 \text{ GeV} \) to \( \approx 1 \text{ PeV} \) can plausibly be produced. Equation (16) also suggests that past energetic SNe in the Galaxy can contribute to cosmic rays around the knee (Sveshnikova 2003; Murase et al. 2014), an energy range that can hardly be reached by SN remnants (Bell et al. 2013).

Unfortunately, the covering fraction of the shocks \( f_{\Omega} \) entering Equation (5) cannot be directly inferred from observations in

\[ \footnote{Although the magnetic field behind the shock may increase owing to flux conservation as gas cools and compresses, this is unlikely to result in an appreciably larger \( E_{\text{max}} \) than we have estimated because the ratio of the Larmor radius to the thermal cooling length \( \Delta R_{\text{cool}} \sim 1 / n_\Lambda \) (which controls the radial width of the cooling region at a given temperature/density) will decrease moving to higher densities \( n \gg n_\Lambda \) relative to its value immediately behind the shock.} \]
most cases. To evaluate the uncertainty in its value, we consider two limits: (1) spherically symmetric interaction (maximal $f_{\Omega} = 1$), which for some transients will result in a value of $v_{\text{th}}$ estimated from Equation (5) that is smaller than the average expansion velocity of the ejecta as measured by optical spectroscopy, $v_{\text{ej}}$; and (2) a covering fraction $f_{\Omega} \leq 1$ chosen such that $v_{\text{th}} \leq v_{\text{ej}}/2$, which is the smallest allowed value consistent with some characteristic ejecta speed $v_{\text{ej}}$ (since the shock cannot be moving faster than the ejecta accelerating it). In most cases, $v_{\text{ej}}$ should be taken to be the kinetic-energy-weighted average velocity; although the ejecta may contain a tail of much faster ejecta (or which covers a very limited solid angle $f_{\Omega} \ll 1$, e.g., a collimated jet), such shocks may not dominate the total energetics and hence are less relevant to our analysis. These limits define an uncertainty range of $v_{\text{th}}$, which from Equation (16) in turn translates into a range of $E_{\text{max}}$.

2.4. Gamma-Ray Escape

Although neutrinos readily escape the ejecta without being absorbed, gamma rays may have a harder time.

For relatively low energy gamma rays, the dominant source of opacity is Compton scattering off electrons in the ejecta, for which the cross section can be approximated as (Chodorowski et al. 1992)

$$\sigma_{\text{BH}} \approx \frac{3}{8\pi} \alpha \sigma_{T} Z^{2} \left[ \frac{28}{9} \ln(2x) - 218 \right],$$

(18)

where $\alpha \approx 1/137$ and $Z$ is the atomic charge of the nuclei of atomic weight $A$ (not to be confused with the wind-loss parameter). Using Condition (4), the BH optical depth $\tau_{\text{BH}} \equiv \Sigma\sigma_{\text{BH}}/A$ near peak light at photon energies $x \gg 1$ can be written as

$$\tau_{\text{BH}} \approx \frac{c}{v_{\text{ej}}} \left( \frac{\sigma_{\text{BH}}/A}{\sigma_{\text{opt}}} \right),$$

(19)

$$\approx 0.3 \frac{Z_{\text{eff}}^{2} v_{\text{ej}}^{-1}}{A_{\text{eff}}} k_{0.3} f_{\text{BH}},$$

where $f_{\text{BH}}(x) \equiv \left[ \ln(2x) - \frac{109}{42} \right]$ and $Z_{\text{eff}}/A_{\text{eff}}$ is the average effective atomic charge/mass of the ejecta ($A_{\text{eff}} = Z_{\text{eff}} \approx 1$ for H-rich SNe; $A_{\text{eff}} = 2Z_{\text{eff}} \approx 16$ for the oxygen-rich ejecta of stripped-envelope SNe).

Thus, depending on the shock velocity, we see that—at the epoch of peak light and particle acceleration—we can have $\tau_{\text{BH}} \gtrsim 1$ at photon energies $\gtrsim \text{GeV}$ ($\approx 10^{3}$), especially for hydrogen-poor explosions with lower opacity $k \lesssim 0.03$ and metal-rich ejecta with high $Z$.

Gamma-ray photons can also be attenuated owing to $\gamma-\gamma$ pair production with ambient photons (e.g., Cristofari et al. 2020). The optical depth for interaction on the reprocessed light from the transient near peak light can be written as $\tau_{\gamma\gamma} \approx \sigma_{\gamma\gamma} n_{\text{opt}} R_{\text{th}}$, where $n_{\text{opt}} \approx L_{\text{sh}}/4\pi R_{\text{sh}}^{2} c_{\text{opt}}$ is the radiation density, $L_{\text{sh}} \approx L_{\text{pk}}$ is the optical luminosity assuming it to be shock dominated, $\tau_{\gamma\gamma} \approx c/\bar{v}_{\gamma\gamma}$, $\epsilon_{\text{opt}} \approx 3kT_{\text{pk}} = \epsilon_{\text{opt},1}$ 10 eV is the characteristic energy of a UV/optical photon near the shock (where $T_{\text{pk}} \approx \tau_{\gamma\gamma}^{1/4} L_{\text{sh}}^{1/4}/(4\pi^{2} R_{\text{sh}}^{2} c_{\text{opt}})$, and $\sigma_{\gamma\gamma} \approx (3/16)\sigma_{T}$ is the cross section near the pair-production threshold, which occurs for particle energies $E_{\gamma, \text{th}} \approx 2m_{e} c^{2}/\epsilon_{\text{opt}} \approx 0.05 \epsilon_{\text{opt},1}$ TeV. Again evaluated around the epoch of peak light and particle acceleration,

$$\tau_{\gamma\gamma} \approx \frac{27}{512} \Theta_{\text{f}} \frac{m_{p} v_{\text{sh}}^{2}}{c_{\text{opt}}} \sigma_{T} \left( \frac{c}{v_{\text{sh}}} \right) \approx 7 \times 10^{4} \Theta_{\text{f}}^{1/3} k_{0.3}^{1/3} \epsilon_{\text{opt},1}^{-1}.$$

Thus, photons of energy $\gtrsim E_{\gamma, \text{th}} \sim 0.1–1$ TeV will generally be attenuated before escaping.12

2.5. Example Shock-powered Transient

As an example of a shock-powered transient, Figure 2 presents the time evolution of the luminosities (top panel) and cumulative radiated energies (bottom panel) in optical, relativistic protons, neutrinos, and $\gamma$-rays. We consider an SLSN-II event with $L_{\text{pk}} \equiv 10^{50} \text{erg s}^{-1}$, $t_{\text{pk}} = 34$ days, and $v_{\text{ej}} = 8000 \text{ km s}^{-1}$ (Inserra 2019), with a characteristic optical light curve from Inserra (2019). The optical luminosity, which well represents the shock power after $t_{\text{pk}}$, is used to evaluate $v_{\text{ej}}(t)$ and $A(t)$ using Equation (1). To break the degeneracy of the time dependence, we consider two limits, wherein either $v_{\text{ej}}$ or $A$ is assumed to be constant in time. Most curves in the figure correspond to the former limit ($v_{\text{ej}} = \text{const}$), except the black dotted curves in the second and third panels (which assume $A = \text{const}$).

The luminosity of relativistic protons, $L_{p} \equiv L_{\text{rel}}$, is computed using Equation (6) with $f_{\text{sh}} = 1$ and $\epsilon_{\text{rel}} = 0.01$ (see Section 3).

As proton–proton interactions roughly equally split the proton energy into neutrinos and electromagnetic energy ($\gamma$-rays and electrons), the neutrino and $\gamma$-ray luminosities are evaluated as

$$L_{\nu} \approx \frac{1}{2} L_{p} f_{\text{pp}}$$

(20)

and

$$L_{\gamma} \approx \frac{1}{3} L_{p} f_{\text{pp}} \exp(-\tau_{\gamma}),$$

(21)

respectively. The factor 1/2 arises because charged pions produced with roughly 2/3 probability in a $p$–$p$ interaction and about three-quarters of their energy is carried away by neutrinos. The other one-quarter is carried away by electrons. These electrons, with energy $\approx 50(E_{p}/1 \text{PeV}) \text{ TeV}$, lose most of their energy through synchrotron radiation, as their inverse Compton process with optical photon background is suppressed owing to the Klein–Nishina effect. The factor 1/3 in $\gamma$-ray spectrum is because neutral pions are produced with roughly 1/3 chance and all their energy is carried by photons.

The maximum proton energy, $E_{\text{max}}$ is computed from Equation (15) for $\epsilon_{B} = 0.01$, and the radiated neutrino energy is estimated as $E_{\nu} \approx 0.05 E_{p}$. Here $f_{\text{pp}} = 1 - \exp(-\tau_{\text{pp}})$

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12 Gamma rays with lower energies can in principle pair-produce on harder UV/X-rays of energy $\approx kT_{\text{sh}}$ (Equation (2)) that exist immediately behind the shocks. However, due to the thin geometric extent of the cooling layer and the lower number density of high-energy photons carrying the same luminosity, this form of attenuation is subdominant compared to other forms of opacity in this energy range (e.g., inelastic Compton scattering; as also noted in Murase et al. 2011); see Figure 3.
Figure 2. Example shock-powered optical transient, showing the dependence of various quantities related to relativistic-particle acceleration as a function of time since explosion. From top to bottom: (1) luminosities of shocks (reprocessed optical emission) and their observable signatures (relativistic protons, neutrinos, and γ-rays, in the latter case for different assumptions about the ejecta composition); (2) maximum accelerated proton energy and emitted neutrino energy; (3) optical depths, of protons to p-p interactions, 1 GeV and 1 TeV γ-rays (shown separately for H-rich and H-poor shocked medium as denoted by different values of the ejecta composition Z); and (4) cumulative radiated energy in the form of optical emission (gray), relativistic protons (black), neutrinos (blue dashed), and γ-rays (red and orange dashed–dotted). We have adopted a canonical Type II SLSN light curve from Inserra (2019). Dotted lines in the second and third panels show how the evolution of $E_{\text{max,pp}}$ and the p-p interaction optical depth would instead change if the luminosity evolution were driven by a decelerating shock (decreasing $v_{\text{sh}}$) into a medium of constant wind parameter $A$. The true evolution of the shock properties likely lies between these two limits, i.e., $E_{\text{max,pp}}$ relatively constant in time. Relativistic-particle acceleration, and thus γ-ray/neutrino emission, is not expected prior to the optical peak (shown as a gray shaded region) owing to the shock being radiation at high optical depths.

Figure 3. Optical depth of the ejecta to γ-rays as a function of the gamma-ray energy $E_{\gamma}$, evaluated for conditions corresponding to the example shock-powered transient in Figure 2 around the epoch of peak light and particle acceleration, $t \approx t_{pk}$. Blue dashed lines show the BH optical depth for two different assumptions about the nuclear composition of the ejecta ($Z = 1, 8$), while a gray dashed–dotted line shows the effective optical depth due to Compton scattering. Solid, thick doted, and thin dotted black lines show the optical depth to γ-γ pair production off of the optical, X-ray, and a TDE-like (peaked around 100 eV) thermal radiation, respectively. For comparison, the red solid line indicates $\tau_{\gamma} = 1$. so the pion production efficiency at these energies is instead $f_{pp} = 1 - \exp(-t_{\text{dyn}}/t_{pp}) = 1 - \exp(-\tau_{t_{pk}}/\tau_{\text{sh}})$. The correction to $f_{pp}$ barely affects the neutrino flux calculation since $\tau_{t_{pk}} > 1$ around the peak time when most neutrinos are produced. It may, however, significantly increase the γ-ray flux in a scenario where most γ-rays are produced at late time.

Figure 3 shows the optical depth of the ejecta as a function of gamma-ray energy $E_{\gamma}$, at an epoch around optical peak ($t \approx t_{pk}$) for each of the processes described above. The third panel in Figure 2 shows the optical depth of the ejecta to gamma rays of energy $E_{\gamma} = 1$ TeV and $E_{\gamma} = 1$ GeV, the latter for two different choices of the nuclear composition of the ejecta, $Z = 1$ and 8 (corresponding roughly to hydrogen-rich and hydrogen-poor explosions, respectively). Due to the bright optical background, TeV γ-rays are heavily attenuated by pair production in the first ~90 days. After that, optical photons fall below the energy threshold needed for pair production with TeV photons. The attenuation of GeV γ-rays is dominated by the BH process. Depending on the composition of the external medium, the source is γ-ray dark in the first ~50 to ~100 days. As a result, although the total radiated energy in neutrinos is a fixed fraction $\sim c_{\text{ref}}/2$ of the total optical output and saturates quickly around $t_{pk}$ (bottom panel of Figure 2), the total radiated energy in gamma rays is greatly suppressed, particularly in the case of hydrogen-poor external medium ($Z_{\text{eff}} = 8$).

3. Particle Acceleration in Novae

Classical novae observed simultaneously via their optical and high-energy gamma-ray emission offer an excellent opportunity to test and calibrate our understanding of particle acceleration at internal radiative shocks. The brightest novae achieve peak optical luminosities $L_{pk} \sim 10^{38} - 10^{39}$ erg s$^{-1}$ and light curves that rise on a timescale $t_{\text{pk}} \sim \text{days} \sim 10^{5} \text{s}$ (Gallagher & Starrfield 1978). The tight temporal correlation between the optical and gamma-ray luminosities (Li et al. 2017; Aydi et al. 2020)
strongly suggests that much of the optical luminosity is powered by internal radiative shocks (Metzger et al. 2014a), i.e., $L_{pk} \approx L_{sh}(t_{pk})$. Using Equations (4) and (5) with a characteristic covering fraction of the external medium $f_\text{c} = 0.2$ (e.g., Chomiuk et al. 2014; Derdziński et al. 2017) and $\kappa_{\text{opt}} = 0.3 \text{cm}^2 \text{g}^{-1}$, we derive a value $v_{sh} \approx 500 \text{km s}^{-1}$, which is reasonable from optical spectroscopy. We also find $A \equiv \dot{M}/(4\pi v_{sh}) \approx c t_{pk}/\kappa_{\text{opt}} \approx 10^3 A_\odot$; taking $v_{sh} \approx v_{sh}$, the latter corresponds to a mass-loss rate $\dot{M} \sim 10^{25} \text{ g s}^{-1}$ and hence a total mass ejection $M_{pk} \sim 10^{-4} - 10^{-3} M_\odot$, broadly consistent with that inferred by nova modeling (Gehrz et al. 1998).

In detail, the simplified setup laid out in Section 2 for explosive transients is not wholly applicable to novae because much of the total radiated shock energy occurs after some delay with respect to the optical rise time $t_{pk}$. Shock interaction in novae is in most cases likely driven by a fast wind from the white dwarf that is observed to accelerate in time, resulting in higher ejecta speeds and shock velocities $v_{sh} \gtrsim 10^3 \text{km s}^{-1}$ being reached on the timescale of $\sim \text{weeks} \gg t_{pk}$ over which most of the gamma-ray emission occurs (Ackermann et al. 2014). This kind of wind-powered transient behavior is distinct from singular explosive transients like SNe, for which in general there is no sustained long-lived activity from a “central engine,” such that $v_{sh}$ and hence $L_{sh}$ for most external medium density profiles) only declines at times $t \gtrsim t_{pk}$.

Nevertheless, insofar as we have good evidence that the gamma-ray emission from novae is powered by internal radiative shocks in the calorimetric limit (Metzger et al. 2015), we can use the properties of the particle acceleration as inferred from their observed gamma-ray luminosity and energy spectrum to guide our expectations for shock-powered transients more generally. Figure 4 shows models of hadronic gamma-ray emission from radiative shocks calculated based on the models of Vurm & Metzger (2018) and applied to the time-integrated gamma-ray spectrum of the nova ASASSN 16ma (Li et al. 2017). The model assumes that protons are injected at the shock with a number distribution $dN_p/dp \propto p^{-q}$, where $p = \beta m_p c^2$ is the proton momentum and $q$ is a power-law index. The normalization of the accelerated proton energy, $E_{\text{rel}}$, is assumed to be proportional to the radiated optical fluence according to $E_{\text{rel}} = E_{\text{rel}}(E_{\text{opt}})$. Some models also include an exponential cutoff above the momentum $p_{\text{max}} = E_{\text{max}}/c$ corresponding to some maximum proton energy, $E_{\text{max}}$.

As shown in Figure 4, several of the models can in principle reproduce the main features of the observed spectrum, particularly the overall spectral shape, including the deficit in the lowest-energy bin $\leq \text{few} 100 \text{ MeV}$. This low-energy turnover arises naturally in hadronic models owing to the pion creation threshold corresponding to their rest energy $\sim 135 \text{ MeV}$; the spectrum in the LAT range is produced mainly by $\pi_0$ decay, which generates few photons below this energy. The decay of charged pions $\pi_\pm$ also generates electron $-\pi_\pm$-positron pairs of comparable numbers and energies; those contribute mainly in the hard X-ray and MeV domain by inverse Compton and bremsstrahlung, partially suppressed by Coulomb losses.

$\gamma$ This unusual time evolution of the shock power in novae also explains why it is possible for $\sim \text{GeV}$ gamma rays to evade the constraints set by BH absorption (Equation (18)) and escape from the ejecta. However, the delayed onset of gamma-ray emission relative to the optical peak seen in some novae (the earliest gamma-ray data in ASASSN 16ma provides a striking example; Li et al. 2017) may point to absorption occurring around $\sim t_{pk}$ even in these systems.

![Figure 4](image-url)

Figure 4. Top panel: models of hadronic gamma-ray emission from nonrelativistic radiative shocks (Vurm & Metzger 2018) fit to the time-integrated Fermi LAT spectra of the classical nova ASASSN 16ma (Li et al. 2017; black points). The models make different assumptions about the injected population of relativistic protons at the shock, such as the power-law index $q$ of their momentum spectrum and the high-energy cutoff, $E_{\text{max}}$. For low values of $q \approx 2-2.2$ (with $E_{\text{obs}}(dN_{\gamma}/dE_{\gamma}) \sim \text{const}$) the data require a modest $E_{\text{max}} \lesssim 30 \text{ GeV}$, while for larger $q \gtrsim 2.4$ the value of $E_{\text{max}}$ is essentially unconstrained (we take $E_{\text{max}} = 5 \text{ TeV}$ in the $q = 2.7$ model). Bottom panel: neutrino spectra for the $E_{\text{max}} = 5 \text{ TeV}, q = 2.7$ model shown in the top panel.

Although some fits are formally better than others, these differences should not be taken too seriously considering the many simplifications going into the analysis, such as fitting a single set of shock conditions to observations that have been time-averaged over several weeks ($\approx$many cooling timescales in which the shock properties are likely to evolve). In all cases we find $\epsilon_{\text{rel}} \approx (2-4) \times 10^{-5}$, consistent with the expected acceleration efficiency from corrugated quasi-parallel radiative shocks (Steinberg & Metzger 2018). This is also consistent with upper limits from the Type IIIn interacting SN 2010jl from Fermi LAT, which Murase et al. (2019) use to constrain $\epsilon_{\text{rel}} \lesssim 0.05-0.1$.

Figure 4 shows that there exists a significant degeneracy between the value of $q$ and the high-energy cutoff $E_{\text{max}}$. Models with flatter injection (low $q$) require a high-energy cutoff, while for those with steep injection (high $q$) the value of $E_{\text{max}}$ is essentially unconstrained. For instance, both the
combinations \((q = 2.4, E_{\text{max}} = \infty)\) and \((q = 2, E_{\text{max}} \approx 25\ \text{GeV})\) can fit the data (again, within uncertainties accounting for the simplifying assumptions of the model).

Despite the above-mentioned degeneracy, there exist theoretical reasons to favor the low \(q\) intrinsic cutoff (low \(E_{\text{max}}\)) cases. First, for high Mach number shocks \((M \gtrsim 30–100\) in novae) diffusive shock acceleration predicts a spectrum \(q \approx 2\) (e.g., Blandford & Ostriker 1978; Caprioli & Spitkovsky 2014a). Although the spectrum can be steepened by nonlinear effects due to cosmic-ray feedback on the upstream (e.g., Malkov 1997), this is unlikely to be important given the low \(f_{\text{ed}} \lesssim 1\%\). Applying Equation (16), we find values of \(E_{\text{max}} \approx 1–100\ \text{GeV}\) for characteristic parameters \(L_{\text{pk}} \approx 10^{38–39}\ \text{erg s}^{-1}, v_{\text{sh}} \approx 500–2000\ \text{km s}^{-1}, \kappa_{0.3} \approx 1, Z \approx 1,\) and \(s_{B} = 0.01,\) consistent with the low-\(E_{\text{max}}\) models in Figure 4. In principle, the high-energy cutoff in nova gamma-ray spectra may not be intrinsic, but instead arise owing to \(\gamma\gamma\) pair creation on the nova optical light (Metzger et al. 2016); however, this environmental cutoff should not set in until \(E_{\gamma} \gtrsim 30\ \text{GeV}\) (Figure 3), corresponding to an equivalent \(E_{\text{max}} \approx 300\ \text{GeV}\) typically higher than needed to fit the data in Figure 4.

Even if proton acceleration in nova shocks “fizzles out” at \(E_{\text{max}} \lesssim 100\ \text{GeV},\) otherwise similar shocks, but scaled to the much higher luminosities needed to power energetic extragalactic transients, could reach significantly higher \(E_{\text{max}} \propto L_{\text{pk}}^{1/2}\) with a flat spectrum \(q \approx 2.\) Motivated thus, in the sections to follow we apply the assumption of moderate \(q \approx 2.2\) and \(E_{\text{max}}\) following Equation (16) (for the same value of \(s_{B} = 0.01\) “calibrated” to match the gamma-ray emission from novae) to extragalactic transients.

### 4. Applying the Calorimetric Technique to the Transient Zoo

In this section we apply the basic methodology of Section 2 to a large range of possible shock-powered transients (several already mentioned in the Introduction) in order to place an upper limit on their high-energy gamma-ray and neutrino emissions. We do this using exclusively observed properties of each class under the assumption that 100% of their optical fluence is shock powered and the particle acceleration properties follow those measured from classical novae.

#### 4.1. Observed Properties of Transient Classes

Table 1 and Figure 5 summarize a diverse list of known or suspected nonrelativistic shock-powered optical transients. For each class, we provide the range of measured or assumed quantities, including the local volumetric rate \(\dot{\mathcal{R}}_{\odot}\), peak luminosity \(L_{\text{pk}}\), peak timescale \(t_{\text{pk}}\), (kinetic-energy-weighted) ejecta velocity \(v_{\text{ej}}\), radiated optical energy \(E_{\text{opt}}\) (in many cases approximated as \(\sim L_{\text{pk}}t_{\text{pk}}\)), and average charge of nuclei \(Z_{\text{eff}}\) in the ejecta/external medium. In the final column we also provide a qualitative indicator of our confidence that shock interaction (possibly hidden) plays an important role in powering a sizable fraction of each transient class. Before proceeding, we go into some details on the various transient classes entering this table. We also discuss how we expect the rate to evolve with cosmic redshift \(z\), as this will enter our background calculations below. Our main goal is to quantify the total production rate of optical light from different transient classes in order to place constraints on the neutrino background.

For LRNe from stellar mergers, Kochanek et al. (2014) find a peak luminosity function \(L_{\text{pk}}(dN/dL_{\text{pk}}) \propto L_{\text{pk}}^{-0.4 \pm 0.3}\). Coupled with the tendency for the more luminous LRNe to last longer (Metzger & Pejcha 2017), this suggests a roughly flat distribution of radiated optical energy, i.e., \(E_{\text{opt}}(dN/dE_{\text{opt}}) \sim \text{const}\). As an example to nail the normalization, consider V838 Mon (Munari et al. 2002; Tyndela et al. 2005), which peaked at a luminosity \(L_{\text{pk}} \sim 4 \times 10^{39}\ \text{erg s}^{-1}\) on a timescale \(t_{\text{pk}} \sim 40\) days, corresponding to a total optical output \(E_{\text{opt}} \sim 10^{40}\ \text{erg}\). Kochanek et al. (2014) estimate a rate of V838 Mon–like transients of 0.03 yr\(^{-1}\) in the Milky Way. Taking a volumetric density of \(L_{\odot}\) galaxies in the local universe of \(\sim 0.006\ \text{Mpc}^{-3}\), we estimate the local rate of V838 Mon–like LRNe of \(\mathcal{R}(z = 0) \sim 2 \times 10^{5}\ \text{Gpc}^{-3}\ \text{yr}^{-1}\). A more detailed analysis would include an integration of the rates over the distribution of galaxy masses and star formation rates (SFRs), but given the significant uncertainty already present in the galaxy rate, we neglect this complication here. Since the progenitor of V838 Mon was a relatively massive star binary (\(\sim 5–10\ M_{\odot}\)) with a short lifetime, the LRN rate will roughly trace the SFR with redshift.

For classical novae, the estimated Milky Way rate is \(\sim 20–70\ \text{yr}^{-1}\) (Shafter 2017). Again using the \(z = 0\) density of \(L_{\odot}\) galaxies, we find a volumetric nova rate of \(\sim (1–5) \times 10^{8}\ \text{Gpc}^{-3}\ \text{yr}^{-1}\). Likewise, at least in irregular and spiral galaxies (which make up an order-unity fraction of stellar mass in the universe), the rate of novae is believed to trace star formation (e.g., Yungelson et al. 1997; Chen et al. 2016); hence, to zeroth order novae should also trace the cosmic SFR.

For TDE flares, van Velzen (2018) find a peak luminosity function \(L_{\text{pk}}(dN/dL_{\text{pk}}) \propto L_{\text{pk}}^{-1.5}\), which is dominated by the lowest-luminosity events. The total TDE rate is uncertain, but a value of \(\sim 10^{-4}\ \text{yr}^{-1}\) per \(L_{\odot}\) galaxy is consistent with observations (van Velzen 2018) and theory (Stone & Metzger 2016); however, the observed preference for poststarburst galaxies is not understood; Arcavi et al. 2014; Graur et al. 2018; Stone et al. 2018).

For SNe, we consider separately all core-collapse SNe (CCSNe), which are dominated by SNe II with typical values \(L_{\text{pk}} \approx 10^{52}\ \text{erg s}^{-1}\) and \(t_{\text{pk}} \approx 100\) days, corresponding to a total radiated output \(E_{\text{opt}} \approx 10^{50}\ \text{erg}\). The SN II subclass shows clear evidence for shock interaction, but not necessarily always at epochs that allow one to conclude that it is dominating the total optical output of the SN (though more deeply embedded shock interaction could be at work during these events). Following Li et al. (2011), we take the rate of SNe II to be 8.8% of the total CCSN rate.

For SLSNe, roughly defined as SNe with peak absolute g-band magnitude \(M_{g} < -19.8\) (Quimby et al. 2018), we take rates of \(10–100\ \text{Gpc}^{-3}\ \text{yr}^{-1}\) and \(70–300\ \text{Gpc}^{-3}\ \text{yr}^{-1}\) for Type I and II, respectively (Quimby et al. 2013; Gal-Yam 2019; Inserra 2019). We do not distinguish between the “slow” and “fast” subclasses of SLSNe I, despite their potentially different physical origins. A detailed analysis of the luminosity function of SLSNe remains to be performed; however, from the reported population one roughly infers \(dN/dL_{\text{pk}} \propto L_{\text{pk}}^{-\alpha}\) with \(\alpha \approx 1\), and hence we pair the events with the lowest (highest) optical fluence with those of the highest (lowest) rate in calculating the fluence rate below.
As the name “FBOT” suggests, FBOTs are rapidly evolving luminous blue transients that can reach peak luminosities similar to SLSNe. Coppejans et al. (2020) present a summary discussion of FBOT rates. For all FBOTs with peak $g$-magnitude in the range $M_g \lesssim -16.5$ ($L_{pk} \gtrsim 10^{43}$ erg s$^{-1}$), Drout et al. (2014) find a rate at $z < 0.6$ of 4800–8000 Gpc$^{-3}$ yr$^{-1}$. For the most luminous FBOTs with $M_g < -19$ ($L_{pk} \gtrsim 10^{44}$ erg s$^{-1}$), a class including AT2018cow (Prentice et al. 2018), CSS161010 (Coppejans et al. 2020), and ZTF18abvkwlw (the “Koala”; Ho et al. 2020), Coppejans et al. (2020) estimate a rate of $R \sim 700–1400$ Gpc$^{-3}$ yr$^{-1}$ at $z \lesssim 0.2$. Several of the luminous FBOTs show clear radio signatures of shock interaction on large radial scales (Margutti et al. 2019; Coppejans et al. 2020; Ho et al. 2020); the energy source behind the bulk of the optical emission in these events is debated (though Margutti et al. 2019 present evidence that the optical emission in AT2018cow is powered indirectly by reprocessed X-rays). The association of FBOTs with star-forming host galaxies (Drout et al. 2014) again justifies scaling their rate with the cosmic SFR.

A small subset of SNe Ia show evidence for shock interaction between the ejecta of the exploding white dwarf and hydrogen-rich circumstellar material (so-called “Type Ia-CSM”); Hamuy et al. 2003; Chugai & Yungelson 2004; Aldering et al. 2006; Dilday et al. 2012; Bochenek et al. 2018). These events are estimated to accompany between $\sim 0.1\%$ and $1\%$ of SNe Ia, corresponding to a volumetric rate of $\sim 300–3000$ Gpc$^{-3}$ yr$^{-1}$. In addition to the relatively exotic transients above, we also consider the more speculative possibility that even ordinary CCSNe (e.g., Type IIP, Type Ibc) are shock powered at some level (e.g., Sukhbold & Thompson 2017).14 From their explosion models of stripped-envelope stars, Ertl et al. (2020) find that the $^{56}$Ni production in their models is able to explain at best half of the luminosities of Type Ib/c SNe, pointing to an additional energy source in these systems (see also Woosley et al. 2020).

4.2. Derived Properties of Transient Classes

Table 2 lists several derived properties for each of the transient classes in Table 1, including the local (redshift $z \approx 0$) injection rate of optical energy, $E_{\text{opt}}$, and the maximum per-particle energy of shock-accelerated protons, $E_{\text{max}}$. The former

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14 As an extreme example, the H-rich SN iPTF14lvs, although identical to an ordinary IIP in terms of its spectroscopic properties, exhibited a light curve that stayed bright over 600 days (as opposed to the $\sim 100$-day plateaus of most IIP), with at least five distinct peaks (Arcavi et al. 2017). Although initially there we no spectroscopic indications of shock interaction, emission features finally appeared at late times, revealing a dense CSM (Andrews & Smith 2018).
Table 2
Derived Properties of Extragalactic\(^a\) Transients

| Source         | \(\log_{10} \dot{E}_{\text{opt}}\) (erg Mpc\(^{-2}\) yr\(^{-1}\)) | \(f_\text{th, min}\) | \(v_{\text{sh}}\) (10^3 km s\(^{-1}\)) | \(\log(E_{\text{max}}/\text{eV})\) |
|----------------|----------------------------------------------------------|---------------------|--------------------------------|---------------------------------|
| Novae          | 43.2                                                     | 4.0 \times 10^6     | 0.1-3.0                         | <9-13.8                         |
| LRNe           | 42.4                                                     | 1.6 \times 10^3     | 0.1-0.5                         | <9-8.1                          |
| SLSNe I        | 43.0                                                     | 1.3 \times 10^2     | 2.4-10.0                        | 14.4-16.1                       |
| SLSNe II       | 43.5                                                     | 3.6 \times 10^2     | 3.3-10.0                        | 14.6-16.1                       |
| SNe Iin        | 43.5                                                     | 5.2 \times 10^3     | 0.9-5.0                         | 11.1-14.9                       |
| CCSNe          | 43.8                                                     | 4.8 \times 10^2     | 1.1-3.3                         | 11.2-14.0                       |
| TDE            | 45.0                                                     | 4.9 \times 10^3     | 2.5-15.0                        | 14.7-17.4                       |
| FBOT           | 43.4                                                     | 1.0 \times 10^3     | 3.0-30.0                        | 14.9-18.3                       |
| Lum. FBOT      | 43.6                                                     | 2.4 \times 10^2     | 8.7-30.0                        | 16.5-17.4                       |
| Type Ia-CSM    | 43.5                                                     | 1.6 \times 10^2     | 2.5-10.0                        | 13.9-15.7                       |

Note.
\(\text{\(a\) LRNe and novae are also frequent Galactic transients.}\)

The maximum proton energy, \(E_{\text{max}}\), is calculated following Equation (15) with \(Z = 1\). Although \(E_{\text{max}} \propto Z\) and hence could be larger for hydrogen-poor CSM, the energy per nucleon \(E_{\text{max}}/A\) is roughly independent of \(Z \approx A/2\). As discussed after Equation (16), the uncertainty in the shock covering fraction \(f_\text{th}\) results in a corresponding uncertainty in \(v_{\text{sh}} \leq v_{\text{ej}}/2\) (and hence \(E_{\text{max}}\)). A smaller \(f_\text{th}\) requires a larger \(v_{\text{sh}}\) to generate the same optical luminosity. For transient classes with a range of peak luminosity and peak time, the higher (lower) bounds of \(L_{pk}\) are matched with the lower (higher) bounds of \(t_{pk}\) to derive the permitted range of \(v_{\text{sh}}, f_{\text{th}},\) and \(E_{\text{max}}\).

4.3. \(\dot{E}_{\text{opt}}\) and \(E_{\text{max}}\) Required by Neutrino Observation

The total neutrino flux contributed by sources over cosmological distances can be calculated by (Waxman & Bahcall 1999)

\[
\Phi(E_\nu) = \frac{R_0}{4\pi} \int dz \frac{c}{(1 + z)^2} H(z) f(z) \left( E_\nu^3 \frac{dN}{dE_\nu} \right)(z),
\]

where \(E_\nu = E_{\nu}(1 + z)\) is the redshifted neutrino energy, \(H(z) = H_0\left(1 + z\right)^2 + \Omega_m z^2\) is the Hubble constant at redshift \(z\), \(R_0\) is the rate of the transient in the local universe, and \(f(z)\) describes the source evolution, which equals the source rate at redshift \(z\) to that at today, \(f(z) = R(z)/R_0\). As the transient classes in Table 1 approximately follow the SFR, we adopt the \(f(z)\) from Hopkins & Beacom (2006). We adopt a standard cosmology with \(H_0 = 67.4\) km s\(^{-1}\) Mpc\(^{-1}\) and \(\Omega_m = 0.315\) (Planck Collaboration et al. 2020).

Each transient event provides a total neutrino energy \(E_\nu^*\) (\(dN/dE_\nu\) \(\approx (1/2)f_{pp} E_\nu^2 dN/dE_\nu\)), where \(dN/dE_\nu\) and \(dN/dE_\nu\) are the number distributions of neutrinos and relativistic protons, respectively. This expression is obtained by integrating Equation (19) over the lifetime of a transient. As Equation (9) suggests that \(p-p\) interactions are generally efficient at the peak time, below we take the pion production efficiency \(f_{pp} = 1\). Assuming that accelerated protons follow a power-law spectrum, \(dN/dE_\nu \propto E_\nu^{-q}\), and that the \(\epsilon_\text{rel}\) fraction of the shock power is deposited into relativistic particles as described in Equation (6), Equation (22) can be rewritten as

\[
\Phi(E_\nu) = \frac{R_0}{8\pi} \epsilon_\text{rel} \Phi_{E_\nu} \int dz \frac{c f(z)}{H(z)} (1 + z)^{-q},
\]
with a prefactor

$$F_q \equiv \begin{cases} (q - 2)(20 E_v/E_{p,\min})^{2-q} & \text{if } q > 2 \\ \log(E_{\text{max}}/E_{p,\min}) & \text{if } q = 2 \end{cases}$$

(25)

accounting for the integrated proton energy above $E_{p,\min}$. For $E_{p,\min} \approx 1$ GeV, $E_{\text{max}} \approx 10$ PeV, and $E_v \approx 100$ TeV, $F_q \approx 6.2 \times 10^{-2}$, $1.1 \times 10^{-2}$, and $1.2 \times 10^{-3}$ for $q = 2, 2.2,$ and 2.4, respectively. The energy power-law index $q$ is equal to the momentum distribution index $q$ ($dN/dp \propto p^{-q}$) for relativistic particles ($E_p \approx pc$), such that values $q \approx 2–2.4$ are motivated by both the theory of diffusive particle acceleration and direct observations of novae (Section 3, Figure 4).

The neutrino flux as measured by IceCube is $\Phi_{\nu,e,\bar{\nu}} \approx (4–6) \times 10^{-8}$ GeV cm$^{-2}$ s$^{-1}$ sr$^{-1}$ at $E_\nu = 100$ TeV (Schneider 2019; Stettner 2019). To meet the observed diffuse neutrino flux, Equation (24) poses a lower limit to $E_{\text{opt}} R_0$, for given $\epsilon_{\text{rel}}$ and $q$, following the argument connecting optical emission to non-thermal emission (Equation (6) and surrounding discussion),

$$\epsilon_{\text{rel}} E_{\text{opt}} R_0 \approx 5 \times 10^{44} \left( \frac{F_q}{f(q = 2)} \right)^{-1} \left( \frac{\xi}{3} \right)^{-1} \times \left( \frac{\Phi_{\nu,\text{tot}}}{4 \times 10^{-5} \text{ GeV cm}^{-2} \text{s}^{-1} \text{sr}^{-1}} \right) \text{erg Mpc}^{-3} \text{yr}^{-1},$$

(26)

where $\xi \equiv \int dz f(z) H(z)^{-1}(1 + z)^{-\nu}/t_H$ (as first defined in Waxman & Bahcall 1999 with $q = 2$), $t_H = \int dz H(z)^{-1}(1 + z)^{-1}$ is the age of the universe, and $\xi \approx 3$ for a star-forming-history-like $f(z)$.

Figure 6 compares the maximum proton energy injection rate $E_{\text{opt}} R_0$ of various transients derived in Section 224.2 and the lower limit assuming $q = 2$, $\epsilon_{\text{rel}} = 1$, and $\epsilon_{\text{rel}} = 0.01$ (the latter as inferred from applying the calorimetric technique to novae; Section 3; Figure 4). Figure 6 shows that although a wide range of hypothesized shock-powered transients can accelerate ions to sufficient energies to explain the IceCube background, their neutrino production rates typically fall short by $\gtrsim 2–4$ orders of magnitude in the favored case $\epsilon_{\text{rel}} = 0.01$.

Finally, note that we have estimated neutrino production from proton–proton interaction. Nuclei with mass number $A > 1$ lose energy by both fragmentation and pion production (Mannheim & Schlickeiser 1994), with the latter dominating above $\sim 1$ TeV/A (Kraakau & Schlickeiser 2013). Compared to a proton, a nucleus with charge number $Z$ may gain $Z$ times more energy from the same acceleration zone (Equation (14)), though the energy per nucleon, and hence the energy of their neutrino products, is lower by a factor of $\sim Z/A \sim 1/2$ (see Fang 2015 for a comparison of neutrino production from $A-p$ and $p-p$ interaction). The inelastic cross section of nuclei–proton interaction scales roughly by $A^{-1/3}$ (Schlickeiser 2002), which allows efficient pion production at the peak epoch for most nuclei (Equation (9)). Nuclei–nuclei interaction ($A-A$) would further complicate the secondary spectra compared to $A-p$ or $p-p$ interaction (Fang et al. 2012). On the other hand, as the giant dipole resonance occurs at a lower energy with a larger cross section compared to the photopion interaction (Equation (10)), photodisintegration may dominate over hadronuclear interaction and affect neutrino production. A detailed computation of the competing processes is, however, beyond the scope of this work.

### 4.4. Propagation to Earth: Satisfying the Gamma-Ray Background Constraints

The flux of the diffuse neutrino background observed by the IceCube Observatory (Aartsen et al. 2016; IceCube Collaboration 2020c) is comparable to that of the Fermi LAT IGRB around $\sim 100$ GeV (Ackermann et al. 2015a). To avoid over-producing the IGRB, neutrino sources are suggested to be “hidden” (Berezinsky & Dokuchaev 2001), being opaque to $1–100$ GeV $\gamma$-rays or with hard $\gamma$-ray spectral index $\hat{\nu}_\gamma \lesssim 2.1–2.2$ (Murase et al. 2016).

Around the peak time of a shock-powered transient when most of the high-energy neutrinos are produced, a significant fraction of GeV $\gamma$-rays may be attenuated owing to the BH process, depending on the charge number of the CSM (see Section 2.4; also mentioned by Petropoulou et al. 2017; Murase et al. 2019). Later the CSM becomes optically thin to GeV $\gamma$-rays, but proton–proton interaction is weaker and the shock power is lower. Shock-powered transients therefore emit much less energy in high-energy $\gamma$-rays than in high-energy neutrinos (see bottom panel of Figure 2).

To investigate whether these partially $\gamma$-ray-dark sources satisfy the IGRB constraints, we evaluate the diffuse $\gamma$-ray and neutrino fluxes from shock-powered transients. The emission from an individual source is calculated as in Section 2.4, assuming an effective CSM charge number $Z_{\text{eff}}$ and a proton spectrum with index $q$ and power $I_{\nu,\text{opt}} \approx L_{\nu,\text{soft}} / \epsilon_{\text{rel}}$. The diffuse neutrino flux is then obtained by integrating the emission over a source lifetime and the evolution history of the source population following Equation (22). The diffuse $\gamma$-ray flux is computed by numerically propagating $\gamma$-rays from sources to Earth with Monte Carlo simulations. For the computation we adopt the extragalactic background light model from
Figure 7. Diffuse neutrino and $\gamma$-ray fluxes from shock-powered transients compared to the Fermi LAT IGRB (Ackermann et al. 2015a) and the diffuse neutrino flux of the HESEs (Schneider 2019), $\nu_{\gamma}$ events (Aartsen et al. 2016), and cascade events (IceCube Collaboration et al. 2020c) measured by the IceCube Observatory. The fluxes are computed by integrating the neutrino and $\gamma$-ray emission over a Type II SLSN-like light curve (as in Figure 2) and summing over a source population that follows the star formation history. The gray solid curves assume injected spectral index $q = 2.0$ and $q = 2.4$ (from thick to thin) and an effective CSM charge number $Z_{\text{eff}} = 1$, 1, and 2.5, respectively. The fluxes are normalized by the IceCube HESE observation at 270 TeV. When taking a peak luminosity $L_{\text{opt}} = 10^{50}$ erg s$^{-1}$ and $\epsilon_{\text{rel}} = 1\%$, the normalization corresponds to a local source rate of $N = 1 / 17, 220 \times 10^{5}$ Gpc$^{-3}$ yr$^{-1}$ in each scenario.

4.5. Requirements to Match the Neutrino Background

Although shock-powered transients are promising as gamma-ray-dark sources, the known classes of transients we have considered come up several orders of magnitude short in terms of their energetic production (Figure 6). To reproduce the overall normalization of the neutrino background, the scenarios shown in Figure 7 require a hypothesized transient with $E_{\text{opt}} = 5 \times 10^{50}$ erg and a particle acceleration efficiency $\epsilon_{\text{rel}} = 1\%$ with a (optimistic) local rate of $N = 1 / 17, 220 \times 10^{5}$ Gpc$^{-3}$ yr$^{-1}$ for $q = 2, 2.2$, and $2.4$, respectively.

In other words, we require some transient that is as frequent as CCSNe but emits $\gtrsim 50$ times the optical fluence. Stated more precisely, we require a transient (or sum of transients) that obeys

$$\left(\frac{N}{10^{5} \text{ Gpc}^{-3} \text{ yr}^{-1}}\right)\left(\frac{E_{\text{opt}}}{5 \times 10^{50} \text{ erg}}\right)\left(\frac{\epsilon_{\text{rel}}}{0.01}\right) \sim 1$$

(27)

for $q \approx 2$. Larger values of $q$ would require even larger values of $N$, and/or $E_{\text{opt}}$ as described by Equation (25).

5. Summary and Conclusions

We have introduced a simple technique for combining the observed properties of nonrelativistic optical transients with their maximal high-energy neutrino and gamma-ray outputs in order to constrain their contributions to the IceCube and Fermi backgrounds. Our conclusions may be summarized as follows:

1. A large number of optical transients could in principle be shock powered (Table 1), even if the direct signatures of shock interaction (e.g., emission lines) are hidden at early times. Despite a diversity of dynamics and geometry, a generic feature of their behavior is a shock that propagates outward in time from high to low optical depths through some medium that covers a fraction of the total solid angle (Figure 1).

2. The condition for the creation of a collisionless shock capable of accelerating relativistic ions is similar to that for the escape of optical radiation. Thus, relativistic-particle acceleration commences around the time of optical maximum, $t_{\text{pk}}$, which for most transients is also the epoch at which the majority of the optical radiation energy is released.

3. The calorimetric technique makes use of the fact that at the epoch $\sim t_{\text{pk}}$ the cooling time of both thermal and nonthermal particles (via free–free emission and $p-p$ interactions, respectively) is generically short compared to the expansion time (Equations (8) and (9)). As a result, the energy radiated by nonthermal ions in high-energy neutrinos and gamma rays is directly proportional to the transient’s shock-powered optical energy. The proportionality constant is the ion acceleration efficiency, $\epsilon_{\text{rel}}$ (Equation (6)).

4. Observations of correlated optical and gamma-ray emission in classical novae (e.g., Li et al. 2017; Aydi et al. 2020) enable a proof-of-principle application of the calorimetric technique that probes the properties of ion acceleration at radiative internal shocks under physical conditions similar to those that characterize more luminous extragalactic transients. The ratio of optical to gamma-ray luminosities reveals ion acceleration efficiencies $\epsilon_{\text{rel}} \sim 1\%$, while an analysis of the gamma-ray spectra is consistent with relatively flat injected ion spectra ($q \lesssim 2.4$) and energy cutoff $E_{\text{max}} \sim 30 \text{ GeV}$ (Figure 4).

5. We make a simple estimate for the maximum particle energy accelerated at radiative shocks (Equations (15) and (16)), which, unlike most previous studies, accounts for the thin radial extent of the downstream region due to radiative compression. Applying this formalism to gamma-ray data from classical novae ($E_{\text{max}} \gtrsim 30 \text{ GeV}$) requires magnetic amplification at the shocks, $\epsilon_{B} \sim 10^{-2}$. Assuming a similar magnetic field amplification factor in the shocks of extragalactic transients, we find that many exceed the threshold $E_{\text{max}} \gtrsim 10^{15} \text{ eV}$ needed to generate neutrinos above 50 TeV (Figure 6) and hence contribute to the IceCube diffuse neutrino flux.

6. Due to the high BH optical depth of the ejecta at the epoch of peak neutrino fluence $t_{\text{pk}}$ (Figure 3), we confirm previous suggestions (e.g., Petropoulou et al. 2017; Murase et al. 2019) that shock-powered transients can in principle serve as gamma-ray-hidden neutrino sources
7. Using the inferred energetics and volumetric rate of each class of transient, we calculate its maximal neutrino output, derived under the assumption that 100% of its optical radiation is powered by shocks. Even in this most optimistic case, we find that the classes of known optical transients we have considered are insufficient to explain the IceCube background (Figure 6) unless they produce a hard proton spectrum with index $q \sim 2$ or lower. With $q > 2.2$ they individually fall short by $\gtrsim 2-3$ mag if we adopt a value $\epsilon_{\text{rel}} = 1\%$ calibrated to classical novae. Even making the optimistic assumption that all CCSNe in the universe are 100% shock powered, the normalization of the background is achieved only in the unphysical case $\epsilon_{\text{rel}} \sim 1$.

8. The most promising individual sources are TDEs, but whether the light curves of these sources are powered by shocks (e.g., Piran et al. 2015) or reprocessed X-rays from the inner accretion flow (e.g., Metzger & Stone 2016) is hotly debated. It has been suggested that the TDE rate decreases with redshift (Kochanek 2016), in which case the neutrino flux would be lower than our estimation based on the evolution of the cosmic SFR. For reference, $\xi$ (Equation (25)) decreases from 2.8 for a star formation evolution to 0.6 for a uniform source evolution.

Interestingly, Stein et al. (2020) recently reported that an IceCube neutrino alert event arrived in the direction of a radio-emitting TDE ~180 days after discovery (see also Murase et al. 2020; Winter & Lunardini 2020). The probability of a coincidence by chance is 0.2%-0.5%. No $\gamma$-ray signal was detected by the Fermi LAT, implying that $\gamma$-rays may have been attenuated by the UV photosphere (Stein et al. 2020), similar to what we suggest in this work. However, our model would predict that neutrinos arrive around the peak time of the optical/UV emission of a TDE, which was around a month after discovery for this event.

9. Although we have focused on radiative shocks, which we have shown to characterize shock-powered optical transients near peak light, for a lower CSM density such as encountered at later times and larger radii—the shocks will instead be adiabatic and our calorimetric argument will break down. However, this is unlikely to significantly change our conclusions because, for most CSM density profiles, the total shock-dissipated energy is still dominated by early times, when the shocks are radiative. Furthermore, the efficiency of relativistic-particle acceleration at nonrelativistic, quasi-perpendicular adiabatic shocks may be even lower than in radiative shocks with the same upstream magnetic field geometry owing to the effects of thin-shell instabilities on the shape of the shock front (Steinberg & Metzger 2018).

10. Several of the transient classes considered in our analysis (e.g., FBOTs) have only been discovered and characterized in the past few years. We therefore cannot exclude that another class of optical transients will be discovered in the future that is more promising as a background neutrino source. However, given the stringent requirement on the product of volumetric rate and optical energy fluence placed by Equation (26) to match the IceCube flux, it is hard to imagine that recent or existing synoptic surveys (e.g., ZTF, PanSTARRs) have missed such events completely. One speculative exception would be a source class restricted to the high-redshift universe, in which case the greater sensitivity and survey speed of the Vera C. Rubin Observatory would be required for its discovery. One may also speculate about the existence of a class of optically dark but infrared-bright transients missed by previous surveys (e.g., Kasliwal et al. 2017).

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References
Aartsen, M. G., Abraham, K., Ackermann, M., et al. 2016, ApJ, 833, 3
Aartsen, M. G., Ackermann, M., Adams, J., et al. 2018, Sci, 361, eaat1378
Ackermann, M., Ajello, M., Albert, A., et al. 2014, Sci, 345, 554
Ackermann, M., Ajello, M., Albert, A., et al. 2015a, ApJ, 799, 86
Ackermann, M., Arcavi, I., Baldini, L., et al. 2015b, ApJ, 807, 169
Aldering, G., Antilogus, P., Bailey, S., et al. 2006, ApJ, 650, 510
Andrews, J. E., & Smith, N. 2018, MNRAS, 477, 74
Arcavi, I., Gal-Yam, A., Sullivan, M., et al. 2014, ApJ, 793, 38
Arcavi, I., Howell, D. A., Kasen, D., et al. 2017, Nat, 551, 210
Aydi, E., Sokolovsky, K. V., Chomiuk, L., et al. 2020, NatAs, 4, 776
Beck, A. M., Hanasz, M., Lesch, H., Remus, R.-S., & Stasyszyn, F. A. 2012, MNRAS, 429, L60
Bell, A. R. 2004, MNRAS, 353, 550
Bell, A. R., Schure, K. M., Reville, B., & Giacinti, G. 2013, MNRAS, 431, 415
Berezhzinsky, V. S., & Dokuchaev, V. I. 2001, ApPh, 15, 87
Blandford, R. D., & Ostrikov, J. P. 1978, ApJL, 221, L29
Bochenek, C. D., Dwarkadas, V. V., Silverman, J. M., et al. 2018, MNRAS, 473, 336
Capanema, A., Esmaili, A., & Serpico, P. D. 2020b, arXiv:2007.07911
Capiroli, D., & Spitkovsky, A. 2014a, ApJ, 783, 91
Capiroli, D., & Spitkovsky, A. 2014b, ApJ, 794, 46
Chakraborti, S., Ray, A., Soderberg, A. M., Loeb, A., & Chandra, P. 2011, NatCo, 2, 175
Chen, H.-L., Woods, T. E., Yungelson, L. R., Gilfanov, M., & Han, Z. 2016, MNRAS, 458, 2916
Cheung, C. C., Jean, P., Shore, S. N., et al. 2016, ApJ, 826, 142
Chevalier, R. A., & Fransson, C. 1994, ApJ, 420, 268
Chevalier, R. A., & Irwin, C. M. 2011, ApJL, 729, L6
Chevalier, R. A., & Li, Z.-Y. 2000, ApJ, 536, 195
Chodorowski, M. J., Zdziarski, A. A., & Sikora, M. 1992, ApJ, 400, 181
Chomiuk, L., Linford, J. D., Yang, J., et al. 2014, Nat, 514, 339
Chugai, N. N., & Yungelson, L. R. 2004, AstL, 30, 65
Waxman, E., & Katz, B. 2017, in Shock Breakout Theory, ed. A. W. Alsabti & P. Murdin (Berlin: Springer), 967
Weaver, T. A. 1976, ApJS, 32, 233
Winter, W., & Lunardini, C. 2020, arXiv:2005.06097
Woosley, S. E. 2010, ApJL, 719, L204
Woosley, S. E., Blinnikov, S., & Heger, A. 2007, Natur, 450, 390
Woosley, S. E., Sukhbold, T., & Janka, H. T. 2020, ApJ, 896, 56
Xi, S.-Q., Liu, R.-Y., Wang, X.-Y., et al. 2020, ApJ, 896, L33
Yuan, Q., Liao, N.-H., Xin, Y.-L., et al. 2018, ApJL, 854, L18
Yungelson, L., Livio, M., & Tutukov, A. 1997, ApJ, 481, 127
Zel’dovich, Y. B., & Raizer, Y. P. 1967, Physics of Shock Waves and High-temperature Hydrodynamic Phenomena (New York: Academic)
Zhang, B. T., & Murase, K. 2019, PhRvD, 100, 103004
Zirakashvili, V. N., & Ptuskin, V. S. 2016, APh, 78, 28