What drives the insulating state in ultrathin films of SrRuO$_3$?

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Using density functional calculations we have examined the evolution of the electronic structure of SrRuO$_3$ films grown on SrTiO$_3$ substrates as a function of film thickness. At the ultrathin limit of two monolayers (RuO$_2$-terminated surface) the films are found to be at the brink of a spin-state transition which drives the system to an antiferromagnetic and insulating state. Increasing the film thickness to four monolayers, one finds the surprising result that two entirely different solutions coexist. An antiferromagnetic insulating solution coexists with a metallic solution corresponding to an antiferromagnetic surface and a ferromagnetic bulk. The electronic structure found at the ultrathin limit persists for thicker films and an unusual result is predicted. Thicker films are found to be metallic as expected for the bulk, but the magnetism does not directly evolve to the bulk ferromagnetic state. The surface remains antiferromagnetic while the bulk exhibits ferromagnetic ordering.

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There has been considerable efforts in the search for alternate technologies to the current Si-based technology$^1$. An avenue of research that has been extensively explored is the use of transition-metal perovskite oxides. The interest in these materials stems from their multi-functional properties$^2$. Several of these materials exhibit different types of magnetic ordering, ferroelectricity, charge and orbital ordering, all resulting from a strong interplay between spin, charge and orbital degrees of freedom. A set of interesting members of this class of compounds are those in which the magnetic ordering can be manipulated by an electric field, or the ferroelectric ordering can be manipulated by a magnetic field. Devices based on these materials have been envisioned and this has fueled the study of oxide electronics$^3$. Metallic oxides form an integral part of the oxide-based device technologies, as they would form the connecting electrode material.

Among the perovskite oxides, SrRuO$_3$ is a promising material device applications, which apart from being a metal, although a poor one, also exhibits ferromagnetism up to 160 K$^4$. An additional advantage of SrRuO$_3$ is that correlation effects should be significantly weaker than in the 3$d$ transition-metal oxides. However, when thin films of this material were epitaxially grown on SrTiO$_3$, films less than four monolayers thick were found to be insulating$^5,6$. While the earlier studies reported the loss of ferromagnetic ordering in ultrathin films$^5$, recent studies have reported exchange bias effects which indicate the presence of antiferromagnetic regions$^6$. All in all, the exact mechanism driving the metal-insulator transition in SrRuO$_3$ ultrathin films is still unknown. Could the metal-insulator transition be due to electron correlations, or could it be due to structural effects or extraneous experimental conditions as recently suggested$^7$? The question of whether electron correlations are important in these systems has been investigated experimentally, although there is no consensus. Some experimental studies suggest that electron-correlation effects are important even in the 4$d$ compounds and cannot be ignored$^5,6,10$. Other studies suggest that electron-correlation effects are much weaker and are not at all important in this class of materials$^11$. In order to address these issues, we performed first-principles density functional calculations of thin films of SrRuO$_3$ on a SrTiO$_3$ substrate, and examined the evolution of the electronic structure of the films with respect to the film thickness. We find that electron correlations at the level of GGA+U must be included in order to explain the insulating state. The correlation effects serve the purpose of changing the subtle energy difference between the low-spin and the high-spin states. The transition into the high-spin state at the surface is accompanied by a strong Jahn-Teller-type distortion associated with a $d^4$ configuration with a partially filled $e_g$ states, which drives the system to an insulating state. The choice of $U$ in GGA+U calculations is usually arbitrary. In order to reduce this arbitrariness we calculated $U$ from first-principles using a technique recently developed by one of the authors$^12$. The magnitude of $U$ determined drives the thin films insulating.

SrRuO$_3$ is found to crystallize in an orthorhombic structure with four formula units per unit cell$^13$. The Ru-O-Ru angles in the a-b plane are found to be around 168 degrees. SrTiO$_3$ is found to occur in a cubic structure. The GGA optimized lattice constant of ferromagnetic cubic SrRuO$_3$ is 3.99 Å, while that of cubic SrTiO$_3$ is 3.94 Å. Therefore, there exists a small mismatch between cubic SrRuO$_3$ and SrTiO$_3$. In order to simulate
the ultrathin films of SrRuO$_3$ grown on SrTiO$_3$, we consider a 13 layer symmetric slab containing a central SrO layer, and alternating TiO$_2$/SrO layers along the (001) direction as shown in Fig. 1. The SrRuO$_3$/SrTiO$_3$ structures were constructed to represent SrRuO$_3$ films deposited on the SrTiO$_3$ substrate on a layer by layer mode. In every case we have included 15 Å of vacuum, and we have checked that the results are converged with respect to the thickness of the vacuum layer. The in-plane lattice constant of the TiO$_2$ layers as well as the RuO$_2$ layers is set equal to the equilibrium lattice constant of SrTiO$_3$. As the Ru-O-Ru angles in bulk SrRuO$_3$ deviate from 180 degrees, we have allowed for a GdFeO$_3$ distortion of the RuO$_6$ octahedra and optimised the structure to find the minimum energy solution. Full optimization of the atomic positions is performed. In addition, a $\sqrt{2} \times \sqrt{2}$ reconstruction of the (001) surface was considered, which allowed us to explore the possibility of antiferromagnetic ordering.

The electronic structure of bulk as well as of thin films of SrRuO$_3$ were investigated using the plane-wave pseudopotential implementation of density functional theory and projector-augmented wave potentials in the VASP code \cite{14, 15}. The GGA approximation for the exchange-correlation functional was used. Electron-correlation effects at the Ru sites were included through the GGA+$U$ method within the Dudarev et al. formalism \cite{16}, where $U$ represents the onsite Coulomb interaction strength and $J$ represents the intra-atomic exchange. We used the values of $U = 2.5$ and $J = 0.4$ eV for the Ru 4$d$ states, which were determined for bulk SrRuO$_3$ by using a recently proposed scheme based on the random-phase approximation \cite{12}. Although for the surface the $U$ may be larger due to the reduced screening, we expect the qualitative aspects of the results to remain the same. A special k-point mesh of $6 \times 6 \times 6$ was used for integrations over the the Brillouin zone of the bulk, while a mesh of $4 \times 4 \times 6$ was used for the slab calculations. A denser mesh of $8 \times 8 \times 4$ was used in the density of states calculations for the slabs. A cutoff energy of 250 eV was used for the plane wave basis set.

**How does the electronic structure of bulk SrRuO$_3$ change in GGA+$U$?** We first examine the electronic structure of bulk SrRuO$_3$ as given by the GGA and GGA+$U$ functionals. The comparison between Ru 4$d$ partial density of states (PDOS) for $U = 0$ (GGA) and $U = 2.5$ eV, $J = 0.4$ eV is shown in Fig. 2. The Fermi energy is used as reference by setting it to zero. We note that there is an increase in the exchange splitting for the finite $U$ calculations. In order to examine the origin of the enhanced exchange splitting we plot the up- and down-spin partial density of states in the insets of panels (a) and (b) in Fig. 2. The up-spin density of states which were contributing at the Fermi level now move deeper into the valence band and the system becomes half-metallic as discussed earlier in the literature by Jeng et al. \cite{17}. In the down-spin channel we find that the effect of $U$ is minimal. Hence the increased exchange splitting comes from the movement of up-spin states. Gross features of the partial density of states are otherwise similar and have been previously discussed in the literature \cite{18}. For completeness, we repeat the discussion here in order to contrast with the surface which shows a very unusual electronic structure.

Ru in SrRuO$_3$ has a formal $d^5$ configuration. As the crystal-field splitting is quite large, the electrons occupy the $t_{2g}$ down-spin states after occupying the $t_{2g}$ up-spin states. The system appears to be at the brink of a transition to a half-metallic state with a weak shoulder corresponding to the up-spin states at the Fermi level. It has been pointed out earlier that a larger value of $U$ drives the system into a half-metallic state \cite{17}. The moment on the Ru atom calculated by taking a sphere of radius $0.9$ Å is 1 bohr magneton, significantly reduced from the ionic value. This difference can be explained by the sizeable moments residing on the oxygen atoms.

Having understood the electronic structure of bulk SrRuO$_3$, we proceed by examining the electronic structure of one atomic layer of RuO$_2$ grown on the SrTiO$_3$ substrate. Before discussing the results from the calculations, we first speculate on what to expect. Strong crystal-field anisotropies at the surface are expected to result in a level ordering of doubly degenerate $d_{yz}$ and $d_{xz}$ levels followed by $d_{xy}$ levels. Thus if the system undergoes a transition to a nonmagnetic state the four electrons would go into the $d_{yz}$, $d_{xz}$ levels. This would explain the origin of the insulating ground state. With this simple model in mind, we examined various possible solutions. Along with the ferromagnetic configuration, we considered nonmagnetic as well as antiferromagnetic configurations. For $U = 0$, the ferromagnetic configuration is the ground state, being more stable than the nonmagnetic configuration by 24 meV per RuO$_2$ unit, whereas the antiferromagnetic solution is difficult to converge to. However, for $U = 2.5$ and a $J = 0.4$ eV on Ru, we find that the antiferromagnetic state is more stable by 49 meV per RuO$_2$ unit. Therefore, in every case, magnetism survives at this ultrathin film limit. Most importantly, the transition to the antiferromagnetic state is accompanied by a change in the electronic state from metal to insulator.

**What is the origin of the insulating state?** While it is clear from our results that the insulating state is linked to an antiferromagnetic order, the origin of the insulating state is puzzling, and we rely on an analysis of the projected density of states to explain it. The orbital- and spin-projected density of states of Ru shown in Fig. 3, and the corresponding schematic energy-level diagram shown in Fig. 4. In the up-spin channel we find that the $d_{xy}$, $d_{yz}$ and $d_{xz}$ states have a significant weight in an energy window near $-5$ eV as well as near $0$ eV, and the exact ordering of these $t_{2g}$-derived levels is not very clear. However, when we examine the contributions of
the down-spin counterparts, the ordering becomes clear. The states with $d_{xz}$ and $d_{yz}$ character are at lower energies compared to the state with $d_{xy}$ character.

The origin of this splitting of the $t_{2g}$ levels is clear when one examines the bond lengths in the RuO$_3$ unit at the surface. The in-plane bond lengths are equal to $\sim$1.95-1.96 Å, while the apical oxygen bond length is $\sim$2.13 Å. Hence crystal field effects determine the ordering of the $t_{2g}$ states, with the $d_{xz}$ and $d_{yz}$ levels followed by $d_{xy}$ in each spin channel. This ordering is depicted schematically in the left panel of Fig. 4. These levels interact with the corresponding symmetry levels on the oxygen atoms forming bonding and antibonding states. We illustrate this interaction explicitly for the up-spin $t_{2g}$-derived levels in Fig. 3. As the charge transfer energy between the $d$ states arising from this interaction have significant Ru $d$ character. The hopping interactions however should be strongest for the in-plane $d_{xy}$ orbital. This results in an inversion of the ordering of the bonding levels generated as a result of the interaction.

The strong crystal field that is present at the surface also induces a huge splitting of the $e_g$-derived levels. The $d_{3z^2-r^2}$ states, which were unoccupied in the bulk, are now occupied, while the up-spin $d_{x^2-y^2}$ state lies above the down-spin $d_{xy}$, $d_{yz}$ and $d_{xz}$ states. Hence an unusual ordering of levels emerges from the broken symmetry at the surface.

The next question we asked was what is the energetics involved in driving the unusual level ordering that one finds here. The generation of the large crystal distortion would cost enormous strain energy which we speculate must be compensated by the additional Hund’s intra-atomic exchange present as a result of the high-spin state on Ru being favored. It should be noted that this crystal-field distorted structure exists above a particular value of $U$ for the antiferromagnetic state alone. The nonmagnetic and ferromagnetic solutions do not show such distortion at the two monolayers limit.

Experimentally it is found that the insulating state exists for four atomic layers, so it is important to ask whether the insulating state survives when we have an additional RuO$_2$ layer. This has direct correspondence with experiment as it corresponds to four atomic layers on the exposed TiO$_2$ surface. The TiO$_2$ surface is usually the one exposed in the experiments on which the SrRuO$_3$ films are grown [19]. The Ru $d$-projected PDOS for the atoms at the surface layer as well as at the sub-surface layer are shown in Fig. 5. The system is still found to be insulating. Interestingly the surface Ru atoms show a similar structural distortion as found in the single RuO$_2$ layer case. However, the inner RuO$_3$ layer does not show the same distortion but still is insulating. Thus it is the antiferromagnetic correlations which set in as a result of the crystal distortion of the surface layer which drives the sub-surface RuO$_2$ layer insulating.

In order to probe the thickness at which we have an insulator-metal transition, we investigated the effects of additional RuO$_2$ layers on the electronic structure of the films. Surprisingly, we find that the antiferromagnetic insulating solution is always lower than the ferromagnetic metallic solution for even 8 monolayers. This is far beyond the thickness for which a metal-insulator transition has been observed in experiments. One might suggest that $U$=2.5 eV used in our calculations is too large for the ruthenates. However, we note that the exchange bias effects that has been recently observed in these systems [3] offer us some hints to the solution of this puzzle.

**Could the experimental results be explained by an antiferromagnetic surface and a ferromagnetic bulk (AFMS-FMB)?**

By examining this further we found that the antiferromagnetic solution is actually degenerate with the AFMS-FMB state at the four monolayer limit. The antiferromagnetic solution as we pointed out earlier is insulating, while the AFMS-FMB solution is metallic. Thus, our results indicate that two electronically different states coexist, and that disorder would possibly pin one solution in one region. For thicker films of six or more monolayers we find the AFMS solution to be the most stable. The AFMS-FMB solution we find is the favored solution far away from the ultrathin limit, even for SrRuO$_3$ surfaces.

Overall, thin films of SrRuO$_3$ of 4 monolayer thickness or less are found to be insulating. Examining the electronic structure of ultrathin films with just one RuO$_2$ layer, we find that the Ru atom at the surface undergoes a low-spin to high-spin transition. This rare occurrence of a high-spin state in a 4$d$ oxide results in an antiferromagnetic state being stabilized as the ground state. The antiferromagnetic ordering drives the system insulating. In the limit of 4 monolayers, the antiferromagnetic insulating solution coexists with the solution corresponding to an antiferromagnetic surface and a ferromagnetic bulk (AFMS-FMB). For six-monolayers thick films, we find antiferromagnetic surface and the bulk ferromagnetic solution, which is metallic, to have lower energy. In other words, we find that SrRuO$_3$ surfaces are antiferromagnetic, while the bulk is ferromagnetic.

Hence the electronic structure of systems in the ultrathin limit are very different from the bulk. Crystal-field anisotropies largely determine the properties of ultrathin films. In the case of SrRuO$_3$ we show that a metal to insulator transition takes place as a function of thickness in addition to a ferromagnet to an antiferromagnet transition.

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FIG. 1: A schematic diagram of the slab geometry that was considered. The substrate was fixed at 11 monolayers on which the SrRuO$_3$ films were grown. The present figure corresponds to 2 monolayers of SrRuO$_3$. 

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FIG. 2: The up (solid line) and down (dashed line) spin Ru $d$ partial density of states for bulk SrRuO$_3$ in the ferromagnetic state. The zero of energy corresponds to the Fermi energy.
FIG. 3: The up (solid line) and down (dashed line) spin orbital projected Ru $d$ partial density of states for the surface Ru atom for 2 monolayers of SrRuO$_3$ grown on SrTiO$_3$ calculated for the antiferromagnetic state. The zero of energy corresponds to the top of the valence band.
FIG. 4: The up (solid line) and down-spin (dashed line) crystal field split Ru $d$ levels for the surface atom are shown schematically in the left panel. The interaction of these levels with the O $p$ orbitals (in the right panel) and the ensuing ordering of the up-spin $t_{2g}$-derived levels are shown in the central panel.
FIG. 5: The up (solid line) and down (dashed line) spin Ru $d$ partial density of states for 4 monolayers of SrRuO$_3$ grown on SrTiO$_3$ for (a) sub-surface Ru atom as well as for (b) the surface Ru atom are shown for the antiferromagnetic state. The zero of energy corresponds to the top of the valence band.