A Hybrid PSO Based on Dynamic Clustering for Global Optimization

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Abstract: Particle swarm optimization is a population-based global search method, and known to suffer from premature convergence prior to discovering the true global minimizer for global optimization problems. Taking balance of local intensive exploitation and global exploration into account, a novel algorithm is presented in the paper, called dynamic clustering hybrid particle swarm optimization (DC-HPSO). In the method, particles are constantly and dynamically clustered into several groups (sub-swarms) corresponding to promising sub-regions in terms of similarity of their generalized particles. In each group, a dominant particle is chosen to take responsibility for local intensive exploitation, while the rest are responsible for exploration by maintaining diversity of the swarm. The simultaneous perturbation stochastic approximation (SPSA) is introduced into our work in order to guarantee the implementation of exploitation and the standard PSO is modified for exploration. The experimental results show the efficiency of the proposed algorithm in comparison with several other peer algorithms.

Keywords: Dynamic clustering; Modified PSO; Exploitation and exploration; Dominant particle; Generalized particle; Simultaneous perturbation stochastic approximation (SPSA)

1. INTRODUCTION

The particle swarm optimizer (PSO), which is one of the population-based algorithms and inspired by the social behavior of animals such as fish schooling and bird flocking in nature, was invented by Kennedy and Eberhart (1995). The original PSO model is very simple, and just utilizes velocity and position as the crucial information of the particle. Furthermore, compared with genetic algorithm (GA), simulated annealing (SA), ant colony optimization (ACO) and some other intelligent algorithms, PSO has the advantage of fewer parameters to be adjusted, better robustness, faster convergence and so on. Therefore, PSO has been applied successfully to several optimization problems, such as global optimization problems, scheduling, and other applications in engineering.

In the context of evolutionary computation, the performance of any global optimization algorithms heavily depends on the mechanism of balancing the two conflicting objectives, which are exploiting the best solutions found so far and at the same time exploring the search space for promising solutions. To reach this balance, many modified PSO algorithms have been proposed in recent years. Nevertheless, utilizing PSO to effectively solve the problem of multiple local minimum, especially for the multi-modal and multi-dimensional optimization, is still a challenge for researchers. Therefore, many researchers have subsequently proposed a lot of different improved strategies which can be divided into the following four categories: initialization (Richards and Ventura, 2004), parameter setting (Liu et al., 2016), neighborhood topology (Wang et al., 2013), and hybrid strategy (Moradi and Gholampour, 2016). Kennedy (2000) proposed a PSO that uses a K-means clustering algorithm to identify the centers of different clusters of particles in the population. Li and Yang (2009) proposed a clustering PSO (CPSO) by using a hierarchical clustering method to locate and track multiple peaks in dynamic environments. They also proposed a simplified version of CPSO in (Li and Yang, 2010). However, the above clustering methods used to generate sub-swarms only employ the position information of swarm, and neglected the probability that the fitness of two particles may be significantly different while they are close to each other in space, thus these two particles should belong to different levels of sub-swarms. Furthermore, there is no need using all particles within promising sub-regions to perform exploitation to track the potential local minimum, only a representative particle is enough, and the rest take responsibility for exploration.

This paper introduces a novel dynamic clustering method called Dynamic Clustering HPSO (DC-HPSO) algorithm by taking advantage of position information as well fitness of particles. Through clustering, the entire swarm is divided into several sub-swarms. Simultaneous perturbation stochastic approximation (SPSA) (Spall, 1987) as a simple yet powerful search technique is used to drive the dominant particles to approach to the potential local optimum, while the standard PSO is remedied to help non-dominant particles to fly away from the dominant particle and even out of its cluster so that much more potential local minimum can be found. At the end of given times of clustering, global optimum can be achieved from the set of potential local minima.

The remaining sections of this paper are arranged as following. Section 2 describes the proposed DC-HPSO algorithm. And experimental results are evaluated on standard test functions in comparison with some peer algorithms taken from the
literature in Section 3. Finally, Section 4 summarizes the concluding remarks and future work of this study.

2. PROPOSED ALGORITHM

In the traditional PSO algorithm, each particle has a position and a velocity. $P_{\text{best}}$ and $G_{\text{best}}$ are the best solution for each particle and the global best solution found by all particles so far, respectively. However, $G_{\text{best}}$ does not always guide other particles towards better places if $G_{\text{best}}$ is a false global optimum. This phenomenon becomes much more obvious at the last stage of algorithm because of loss of swarm diversity. Besides, a large amount of exploration may be a time-consuming task as well as increase of the complexity of algorithm. How to efficiently get all the potential local minimums is troublesome matter of exploration. Therefore, we proposed DC-HPSO algorithm to solve this problem.

2.1 Idea of Dynamic Clustering in PSO

The introduction of clustering algorithm into PSO can classify the $N$ particles into $N_d$ clusters. Each cluster is composed of particles with similar property and patterns. The information of different clusters is different, but different information of the particles should be fully utilized to promote evolution of the entire swarm. It is this idea that inspires us to use clustering algorithm to enhance the evolution ability of the entire swarm.

Before introduction of clustering, we should explain some definitions here. Dominant particle, denoted by $y_i$ ($k=1, 2, \cdots, N_d$), has the following features: first, dominant particle should have fitness as good as possible; second, dominant particle can find itself a better position and help other particles in its neighborhood to evolve at next iteration; third, dominant particle has the superiority of evolution. Generalized particle is another case. It has a position $x_i$ with its fitness $f_i$, and denoted by $z_i$, and $z_i=(x_i^T, f_i)^T$. This is to say, $z_i$ is a $(n+1)-dimensional$ vector by adding the fitness. Using $z_i$ instead of $x_i$ as unit pattern for clustering has the following advantage: $x_i$ only represents the spatial information of a particle, when particles with little differences of spatial distance while much difference of function values are clustered into the same cluster, multiple local minima may exist, the dominant particle may not find the best local minima, and exploitation of the dominant particle terminates because local minima of sub-region happens, thus the idea of clustering cannot work in this situation. While $z_i$ can avoid the above problem effectively because it is composed of both spatial information and fitness. Here, $z_i$ is needed to be normalized when clustering in order to avoid a bias.

Now, let $Z=\{z_1, z_2, \cdots, z_N\}$ be a set of $N$ generalized particles, each having $n$ features. A partition clustering algorithm tries to find a partition $C=\{C_1, C_2, \cdots, C_N\}$ of $N_d$ classes. Since the given set can be partitioned in many ways. The most popular way to evaluate similarity between two patterns will be the use of distance measure. The most widely used measurement is the Euclidean distance, which between any two $(n+1)-dimensional$ patterns $z_i$ and $z_j$ is given by,

$$d(z_i, z_j) = \sqrt{\sum_{r=1}^{n+1} (z_{ir} - z_{jr})^2} = \|z_i - z_j\|$$

where $d(z_i, z_j)$ denotes the distance between $z_i$ and $z_j$. In the following, we will give a brief description of the basic $K$-means algorithm. First of all, the initial centers should be given to $N_d$ clusters. Then the samples $\{z_i\}$ should be distributed to the clusters. The distribution can be conducted by the relation, for all $j=1, 2, \cdots, N_d$,

$$z_i \in C_j(t) \text{ if } d(z_i, c_j) < d(z_i, c_k)$$

(2)

The quality of the clustering is determined by the following cost function:

$$E = \sum_{j=1}^{N_d} \sum_{z_i \in C_j} (z_i - c_j)^2$$

(3)

The new cluster centers $C_j(t+1)$, $k=1, 2, \cdots, N_d$, at the $(t+1)$th iterative step, should be computed such that the sum of the squared distances from all points in $C_j(t)$ to the new cluster center is minimized. The measurement which minimizes this is simply the sample mean of $C_j(t)$. Therefore, the new cluster center is given by,

$$c_j(t+1) = \frac{1}{N_j(t)} \sum_{z_i \in C_j(t)} z_i$$

(4)

where $N_j$ is the number of samples in $C_j(t)$. A high level description of the basic $K$-means is presented in Algorithm 1.

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Algorithm 1 K-means Clustering

1: Initialize $N_j$ cluster centers: $c_1, c_2, \cdots, c_{N_d}$ from the normalized set Z;
2: Set $t=0$, and compute $E(t)$ by using (3);
3: do
4: Set $t=t+1$;
5: for ($i=1$ to $N$) do
6: Assign $z_i$ to an appropriate cluster by using (2);
7: end for
8: for ($k=1$ to $N_d$) do
9: Update current $C_k$ by using (4);
10: end for
11: Compute the cost function $E(t+1)$ by using (3);
12: while ($E(t)!\approx E(t+1)$) do
13: end while.

By clustering the generalized particles, particles with closeness of spatial location and little difference of fitness can be probably clustered into the same cluster, and local neighborhood is obtained. We sort the fitness of all particles in the cluster, and choose the current best particle as the dominant particle. Then dominant particle is closest to local minimum and can be seen as a representative of the cluster. It’s a wise choice to use the only dominant particle to move towards the local minimum of the cluster, while other non-dominant particles should try to fly away from the dominant particle, even jump out of this cluster to explore better positions. Based on this analysis, two methods are introduced into exploitation and exploration respectively: one is SPSA because of its simplicity and fast convergence, the other is a modified PSO.

2.2 SPSA Technique for Dominant Particle

One optimization method that has attracted considerable international attention is simultaneous perturbation stochastic approximation (SPSA) method. As motivated by not using direct measurements of the gradient of the objective function
which are often difficult or impossible to obtain. SPSA uses only objective function measurements, which is quite different from methods such as SA or GA. Further, SPSA is especially efficient in high-dimensional problems in terms of providing a good solution at the cost of a relatively small number of measurements of the objective function (Spall, 1987). The SPSA procedure is in the general recursive stochastic approximation form:

\[ x_{k+1} = x_k - a_k \hat{g}_k(x_k) \]  \hspace{1cm} (5)

where \( \hat{g}_k(x_k) \) is the estimate of the gradient \( g(x_k) \) and \( a_k \) is the gain sequence satisfying certain conditions at the \( k \)th iteration. \( \hat{g}_k(x_k) \) for a two-sided finite-difference approximation is given by,

\[ \hat{g}_k(x_k) = \frac{f(x_k + c_k \Delta_k) - f(x_k - c_k \Delta_k)}{2c_k} \Delta_k \]

\hspace{1cm} (6)

where \( \Delta_k \) denotes a vector independently generated from a zero-mean probability distribution, \( \Delta_k \) is the \( i \)th component of \( \Delta_k \), and \( c_k \) denotes a small positive number that usually gets smaller as \( k \) gets larger. The basic SPSA algorithm we implemented is presented in Algorithm 2.

Algorithm 2 SPSA

1: Initialization and coefficient selection for \( x_1, \text{IterNo}, a, c, A, \alpha, \gamma \);
2: for \( k \in [1, \text{IterNo}] \) do
3: Generate zero-mean, \( n \)-dimensional perturbation vector \( \Delta_k \);
4: Generate two small constants: \( a_k = a/(A+k) \) and \( c_k = c/k^2 \);
5: Compute \( f(x_k + c_k \Delta_k) \) and \( f(x_k - c_k \Delta_k) \);
6: Compute pseudo-gradient \( \hat{g}_k(x_k) \) by using (6);
7: Compute \( x_{k+1} \) using (5);
8: End For.

2.3 Modified PSO for Non-dominant Particle

As analyzed earlier, in a fixed cluster, says \( C_k \), where \( y_k \) is the dominant particle, the non-dominant particle should fly away from the dominant particle as far as possible and even out of the real space of this cluster. Thus, non-dominant particle \( x_i \) at time \( t \) would possibly fly along the opposite direction of \( (y_k - x_i) \). Sketch map of iteration for non-dominant particle in its cluster is presented in Fig.1.

![Fig. 1. Sketch map of iteration for non-dominant particle.](image)

Taking the original velocity of \( x_i \) into comprehensive consideration, \( x_i \) can be updated as follows:

\[ v_{ij}^{t+1} = v_{ij}^t + c_1 r_1 (p_i^t - x_i^t) + c_2 r_2 (p_j^t - x_i^t) + s_k (y_j - x_i^t) \]  \hspace{1cm} (7)

\[ x_i^{t+1} = x_i^t + v_i^{t+1} \]  \hspace{1cm} (8)

where \( x_i^t \) and \( v_i^t \) are the \( t \)th dimensional component of the position and velocity of particle \( i \) at time \( t \), respectively; \( p_i^t \) and \( p_j^t \) are the \( t \)th dimensional component of \( P_{best} \) of particle \( i \) and \( G_{best} \) at time \( t \), respectively; \( c_1 \) and \( c_2 \) are positive accelerating constants. \( r_1 \) and \( r_2 \) are two random variables with a uniform distribution in the range of \([0,1]\). \( s_k \) is the inertia weight. \( s_k \) is the gain sequence, which is a positive number that can control the diversity of swarm. A large \( s_k \) can enhance the diversity of swarm, while a small one leads to fast convergence. User can freely choose \( s_k \) from any probability distribution. The modified PSO algorithm for non-dominant particles is described in Algorithm 3.

Algorithm 3 Modified PSO

1: Initialize parameters of \( N, \text{IterNo}, V_{\text{max}}, s_k \);
2: Calculate the fitness and generate \( P_{\text{best}} \) and \( G_{\text{best}} \);
3: for \( (t = 1 \) to \( \text{IterNo} \) \) do
4: for \( (i = 1 \) to \( N \) \) do
5: for \( (j = 1 \) to \( N \) \) do
6: Compute \( v_{ij}^{t+1} \) by using (7);
7: if \( v_{ij}^{t+1} > V_{\text{max}} \) then do
8: \( v_{ij}^{t+1} = V_{\text{max}} \);
9: else if \( v_{ij}^{t+1} < -V_{\text{max}} \) then do
10: \( v_{ij}^{t+1} = -V_{\text{max}} \);
11: End if
12: Compute \( x_i^{t+1} \) by using (8);
13: End for
14: Evaluate the fitness \( f(x_i^{t+1}) \);
15: Update \( P_{\text{best}} \);
16: End for
17: Update \( G_{\text{best}} \);
18: End for.
19: Output \( G_{\text{best}} \).

2.4 Framework of Dynamic Clustering HPSO Algorithm

There are two features making the proposed algorithm dynamic. First, after each time of clustering, particles in each cluster as a sub-swarm exploit or explore according to their roles. Thus, SPSA and modified PSO algorithms need to be performed a number of iterations in each cluster until both satisfy the termination conditions. The next behavior of clustering takes place until all the clusters finish the exploitation and exploration of the current period of clustering. Second, a memory array should be established to store the positions and fitness of the \( N_c \) old dominant particles. At next time of clustering, an old dominant particle determines which newly produced cluster it should belong to. If the new dominant particle is superior to the old one, the old is replaced. If the swarm converges, the \( N_d \) particles will be stored in the same cluster. Therefore, we call it DC-HPSO algorithm. According to the analysis mentioned above, the complete description of DC-HPSO is presented in Algorithm 4.
Algorithm 4 DC-HPSO

1: Initialize parameters $\text{CluIterNo}, N_d$, and initialize particle swarm;
2: Choose $N_d$ particles and memory them into the array of $M^{(0)}$;
3: for ($r=1$ to $\text{CluIterNo}$) do
4: Obtain $N_d$ clusters from set $\{z_i\}$ by using Algorithm 1;
5: for ($k=1$ to $N_d$) do
6: Choose the dominant particle $y^*_k$ from cluster $C_k$;
7: Execute Algorithm 2 for dominant particle $y^*_k$;
8: Execute Algorithm 3 for non-dominant particles;
9: Update dominant particle $y^*_k$ as well as $M^{(r)}_k$;
10: if ($M^{(r-1)}_k$ is superior to $M^{(r)}_k$) then do
11: $M^{(r)}_k = M^{(r-1)}_k$;
12: End if
13: End for
14: Update $G_{best}$ according to $M^{(0)}$;
15: End for.

3. EXPERIMENTS

3.1 Test Functions and Algorithms Compared

The proposed algorithm was applied to the 8 well-known boundary constrained benchmarks (Sun et al., 2004) and other four functions (Bergh, 2002) to evaluate the performance. All test functions were presented in Table 1. The 12 test functions are divided into three groups in terms of their properties: uni-modal and multi-dimensional problem ($f_1 - f_4$), multi-modal and multi-dimensional problems ($f_5 - f_9$), traditional multi-modal and low-dimensional problems ($f_{10} - f_{12}$). For function $f_{11}$, $a(i) = 16(i \mod 5 - 2)$, $b(i) = 16\lfloor i/5 \rfloor - 2$.

Simulations were carried out to achieve a comparative performance analysis of the proposed DC-HPSO algorithm with respect to:

(i). the standard PSO (SPSO) (Richards and Ventura, 2004)
(ii). ARPSO (Riget and Vesterstrøm, 2002)
(iii). Quantum-behaved PSO (QPSO) (Sun et al., 2004)
(iv). Multi-start PSO (MPSO) (Bergh, 2002)
(v). GCPSO (Bergh, 2002)
(vi). RePSO (Evers and Ben, 2009).

3.2 Numerical Results and Comparisons

The comparative study presented on the 12 test functions, focuses on the following performance metrics: (a) the quality of the final solution; (b) the frequency of striking the optima; (c) the convergence of PSO with different parameter settings. In all algorithms, for a particular trial, the same initial positions and velocities were set for all particles, so as to minimize the effect of randomness during comparison. In the simulation, all algorithms used the global version of PSO. Statistics results from 100 trials per benchmark per algorithm over 60,000 function evaluations per trial using swarm size 40, $c_1 = 2.5, c_2 = 1.49618$, which were obtained using Clerc’s constriction models (Clerc and Kennedy, 2002), as for DC-HPSO, $\text{To}IterNo = 50$ in Algorithm 3, $D = 1$, $a = 0.5$, $\alpha = 0.602$, $r = 0.101$ according to literature (Spall, 2005) and $\text{IterNo} = 50$ in Algorithm 2, $\text{ClusterNo} = 30$ in Algorithm 4.

The relative statistics results of DC-HPSO where $s_k$ was set as 0.5, and the number of clusters, $N_d$ was set as 5. Comparisons in terms of quality of the final solutions among functions $f_1 - f_{12}$ were given in Table 2, where “Mean” indicated the mean best solutions found in the last generation and “Std. Dev” denoted the standard deviation. “Best” and “Worst” were the best and worst fitness value throughout 100 trials, respectively. From the results, DC-HPSO outperforms all the other peer PSO algorithms on functions $f_1 - f_{10}$. While for functions $f_{11} - f_{12}$, GCPSO and MPSO outperform the DC-HPSO algorithm by a narrow margin. This means DC-HPSO improves the quality of the average optima in most cases.

Table 1 Numerical test functions

| Test function | D | Range | $f_{\text{min}}$ |
|---------------|---|-------|----------------|
| $f_1 = \sum_{i=1}^3(x_i - 1.24)^2$ | 30 | $[-100,100]^D$ | 0 |
| $f_2 = \sum_{i=1}^3[(100(x_{i+1}-x_i)^2 + (x_i - 1)^2]$ | 30 | $[-30,30]^D$ | 0 |
| $f_3 = \sum_{i=1}^3|x_i| + \prod_{i=1}^3|x_i|$ | 30 | $[-10,10]^D$ | 0 |
| $f_4 = -2\exp\left(-0.2\sqrt{\sum_{i=1}^Dx_i^2}\right) - \exp\left(\frac{1}{4}\sum_{i=1}^D\cos(2\pi x_i)\right) + 20 + e$ | 30 | $[-32,32]^D$ | 0 |
| $f_5 = \sum_{i=1}^3|x_i - 10\cos(2\pi x_i) + 10|$ | 30 | $[-5.12,5.12]^D$ | 0 |
| $f_6 = \sum_{i=1}^Dx_i^2 - \prod_{i=1}^D\cos(\frac{\pi x_i}{2}) + 1$ | 30 | $[-600,600]^D$ | 0 |
| $f_7 = \sum_{i=1}^D(x_i - 1)^2$ | 30 | $[-100,100]^D$ | 0 |
| $f_8 = \sum_{i=1}^Dx_i \sin(\sqrt{|x_i|} + 418.983)$ | 30 | $[-500,500]^D$ | 0 |
| $f_9 = 1 - \exp\left(-2\log(2) + \frac{\sin^2(x_{i+1} - x_i)}{0.0001 + \sin^2(x_{i+1} - x_i)}\right)$ | 1 | $[0,1]$ | 0 |
| $f_{10} = 0.5 + \frac{\sin\left(\frac{\pi(x^{2} + y^{2})}{2}\right)}{1 + 0.001(x^{2} + y^{2})}$ | 2 | $[-10,10]^D$ | 0 |
| $f_{11} = 500 - \frac{1}{0.002 + \sum_{i=1}^{100}\sqrt{(x_{i})^2 + (y_{i})^2}}$ | 2 | $[-65.535,65.535]^D$ | 0 |
| $f_{12} = \left(\sum_{i=1}^{30}i \cos((i + 1)x + i)\right) \left(\sum_{i=1}^{30}i \cos((i + 1)y + i)\right) + (x + 1.42513)^2 + (y + 0.80032)^2 + 186.7$ | 2 | $[-10,10]^D$ | 0 |
Fig. 2. Performance of DC-HPSO for functions $f_1 - f_6$ using different values of $N_d$ : (a) the performance of DC-HPSO for $f_1$, (b) the performance of DC-HPSO for $f_2$, (c) the performance of DC-HPSO for $f_3$, (d) the performance of DC-HPSO for $f_4$, (e) the performance of DC-HPSO for $f_5$, (f) the performance of DC-HPSO for $f_6$.

Table 2 Comparison of algorithms for test functions

| Function | SPSO  | GCPSO  | MPSO  | QPSO  | ARPSO  | RePSO  | DC-HPSO |
|----------|-------|--------|-------|-------|--------|--------|---------|
| $f_1$    | Mean  | 5.89   | 1.75e-027 | 3.95e-024 | 1.35e-022 | 43.201 | 1.75e-004 | 4.44e-032 |
|          | Std. Dev | 1.815  | 1.32e-027 | 1.84e-021 | 4.52e-022 | 2.84e-014 | 0 | 3.45e-032 |
|          | Best   | 2.155  | 7.67e-028 | 7.73e-024 | 1.18e-029 | 43.201 | 1.75e-004 | 0 |
|          | Worst  | 9.745  | 4.93e-027 | 2.55e-018 | 2.17e-021 | 43.201 | 1.75e-004 | 9.86e-032 |
| $f_2$    | Mean  | 61.625 | 21.380 | 9.242 | 36.359 | 29 | 27.353 | 0.118 |
|          | Std. Dev | 13.522 | 2.442 | 1.799 | 32.500 | 0 | 7.430 | 0.321 |
|          | Best   | 35.301 | 15.354 | 2.337 | 20.042 | 0 | 19.885 | 9.27e-007 |
|          | Worst  | 96.976 | 27.528 | 12.683 | 180.119 | 29 | 32.349 | 1.761 |
| $f_3$    | Mean  | 0.380  | 2.30e-004 | 3.49e-007 | 7.21e-024 | 0 | 5.085 | 0 |
|          | Std. Dev | 0.240  | 2.25e-002 | 1.24e-006 | 2.38e-023 | 0 | 0.236 | 0 |
|          | Best   | 0.043  | 1.26e-004 | 9.87e-008 | 2.18e-028 | 0 | 6.212 | 0 |
|          | Worst  | 1.060  | 5.93e-004 | 7.47e-007 | 1.10e-022 | 0 | 4.554 | 0 |
| $f_4$    | Mean  | 1.122  | 1.778 | 2.408 | 3.22e-012 | 8.88e-016 | 0.101 | 8.88e-016 |
|          | Std. Dev | 0.342  | 0 | 0.992 | 5.89e-012 | 0 | 0.745 | 0 |
|          | Best   | 0.597  | 1.778 | 4.387 | 1.47e-013 | 8.88e-016 | 0.073 | 8.88e-016 |
|          | Worst  | 1.881  | 1.778 | 3.488 | 2.89e-011 | 8.88e-016 | 1.324 | 8.88e-016 |
| $f_5$    | Mean  | 66.659 | 46.763 | 52.733 | 20.118 | 0 | 53.452 | 0 |
|          | Std. Dev | 13.316 | 4.877 | 3.466 | 5.196 | 0 | 0.846 | 0 |
|          | Best   | 36.586 | 12.656 | 17.748 | 10.964 | 0 | 51.738 | 0 |
|          | Worst  | 87.967 | 53.768 | 65.546 | 32.837 | 0 | 55.154 | 0 |
| $f_6$    | Mean  | 0.095  | 0 | 0.007 | 0.014 | 2 | 0.015 | 0 |
|          | Std. Dev | 0.042  | 0 | 0.712 | 0.013 | 0 | 0.047 | 0 |
|          | Best   | 0.038  | 0 | 3.75e-003 | 0.002 | 2 | 4.49e-004 | 0 |
|          | Worst  | 0.228  | 0 | 0.355 | 0.051 | 2 | 0.825 | 0 |
| $f_7$    | Mean  | 6.57e-031 | 1.414 | 0.485 | 0.234 | 0 | 1.83e+003 | 0 |
|          | Std. Dev | 3.54e-030 | 0.023 | 0.354 | 0.673 | 0 | 26.458 | 0 |
|          | Best   | 0 | 0.572 | 0.271 | 0.082 | 0 | 1.57e+003 | 0 |
|          | Worst  | 1.97e-029 | 2.019 | 0.759 | 1.343 | 0 | 2.43e+003 | 0 |
| $f_8$    | Mean  | 3.87e+002 | 36.465 | 138.715 | 1.21e+002 | 2.052 | 87.244 | 5.70e-004 |
|          | Std. Dev | 59.535 | 5.424 | 11.411 | 38.052 | 0 | 32.451 | 1.94e-003 |
|          | Best   | 2.27e+002 | 9.536 | 100.423 | 71.314 | 2.052 | 12.932 | 1.29e-009 |
|          | Worst  | 4.16e+002 | 145.197 | 256.764 | 2.18e+002 | 2.052 | 130.178 | 0.01076 |
| $f_9$    | Mean  | 2.96e-004 | 3.73e-003 | 0.899 | 9.34e-004 | 0.029 | 1.271 | 1.97e-015 |
|          | Std. Dev | 0 | 0.056 | 0.464 | 0 | 0 | 0.438 | 0 |
|          | Best   | 2.96e-004 | 1.44e-004 | 0.052 | 9.34e-004 | 0.029 | 0.899 | 1.97e-015 |
|          | Worst  | 2.96e-004 | 0.133 | 1.774 | 9.34e-004 | 0.029 | 2.467 | 1.97e-015 |
| $f_{10}$ | Mean  | 4.69e-004 | 5.80e-128 | 4.04e-123 | 5.31e-004 | 0 | 4.45e-008 | 0 |
|          | Std. Dev | 7.17e-004 | 0 | 7.32e-004 | 5.84e-006 | 0 | 0 | 0 |
|          | Best   | 0 | 5.80e-128 | 4.04e-123 | 8.48e-008 | 0 | 1.23e-014 | 0 |
|          | Worst  | 1.57e-003 | 5.80e-128 | 4.04e-123 | 1.56e-003 | 0 | 5.41e-005 | 0 |
Figure 2 depict the performance of DC-PSO with different number of clusters for 6 selected functions over the evolution process on 100 trial runs, where \( n_s \) was set as 0.5. \( N_d = 1 \) means dynamic clustering is not used for the tests. The experimental results on 6 functions show that our dynamic clustering technique can make the convergence of DC-HPSEO faster (especially when \( N_d \) was set as 5), as well as achieve better results compared with no use of this technique in most cases. The results showed that in most cases, the proposed algorithm could achieve good performance. The advantage of our proposed algorithm may be owing to its local search ability as well as global search ability, since for the optimization problem, trading off between exploration and exploitation during the search is critical to the performance.

4. CONCLUSIONS

This paper presented a novel dynamic clustering HPSO algorithm which firstly clusters the similar particles into the same sub-region and then uses the SPSA and modified PSO algorithms to perform the jobs of exploitation and exploration, respectively. Here, we have achieved this goal by defining dominant particle which can take responsibility for exploitation so that solutions can be refined. Together with the non-dominant particles, which are responsible for exploration, thus the diversity can be maintained effectively. Our approach shows a good performance and outperforms several peer PSO algorithms for most of the studied problems. Hence, we can conclude that our proposed algorithm could achieve a suitable balance between enhancing population diversity and refining solutions. Our experiments are based on specific functions. In the future, experiments in real-world applications will be indispensable for verifying the efficiency of our algorithm.

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