Imaging the two-component nature of Dirac-Landau levels in the topological surface state of Bi$_2$Se$_3$

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Massless Dirac electrons in condensed matter$^{6-8}$ are, unlike conventional electrons, described by two-component wavefunctions associated with the spin degrees of freedom in the surface state of topological insulators$^{5,6}$. Hence, the ability to observe the two-component wavefunction is useful for exploring novel spin phenomena. Here we show that the two-component nature is manifest in Landau levels, the degeneracy of which is lifted by a Coulomb potential. Using spectroscopic-imaging scanning tunnelling microscopy, we visualize energy and spatial structures of Landau levels in Bi$_2$Se$_3$, a prototypical topological insulator. The observed Landau-level splitting and internal structures of Landau orbits are distinct from those in a conventional electron system$^7$ and are well reproduced by a two-component model Dirac Hamiltonian. Our model further predicts energy-dependent spin-magnetization textures in a potential variation and provides a way for manipulating spins in the topological surface state.

Landau quantization associated with the quasi-classical cyclotron motion of electrons in a magnetic field $B$ is a fundamental phenomenon and highlights the difference between conventional and Dirac electrons. In conventional systems, the energy of the $n$th Landau level ($E_n$) is proportional to $(n + \gamma)B$, where $\gamma = 1/2$. Distinct from this, $E_n$ in two-dimensional massless Dirac systems behave as $\propto \sqrt{n|B|}$ (refs 8, 9). Importantly, the Berry-phase effect in Dirac systems eliminates $\gamma$ and ensures the $B$-independence of $E_n$, which is equal to the Dirac-point energy$^{10,11}$. Such an unusual LL sequence has been observed by scanning tunnelling microscopy and spectroscopy (STM/STS) in graphene$^{12,13}$ and in the topological surface state$^{1,14}$.

In addition to the unique energy spectrum, the wavefunctions of Dirac LLs are remarkably different from their conventional counterparts because of their two-component nature$^8$. To study the details of wavefunctions, spectroscopic-imaging STM (SI-STM) is a powerful technique because tunnelling-conductance maps, which include information of the internal structures of wavefunctions through local-density-of-states (LDOS) variations, can be obtained with high energy resolution and high spatial resolution. If the system is uniform, the spatial degeneracy of Landau orbits results in a homogeneous LDOS. The introduction of a potential variation lifts the spatial degeneracy, making it possible to access the localized Landau orbit$^{14-19}$. The Landau orbit drifts along the equipotential lines and the LDOS variation across the orbit contains information of the internal structure of the wavefunction. Indeed, a recent SI-STM study on a conventional two-dimensional electron system revealed the $n$-dependent nodal structure in the wavefunction$^{7}$.

Wavefunction imaging could be even more interesting in Dirac systems, because a potential variation not only lifts the spatial degeneracy of Landau orbits but may also affect the interplay between the two components in the wavefunction. This is particularly important for the topological surface state, where the interplay determines the magnetic properties. Thus, exploring the two-component nature by wavefunction imaging will give us a clue towards developing a novel spin-manipulation protocol. For this, we study LL wavefunctions of a prototypical topological insulator Bi$_2$Se$_3$ using SI-STM.

Figure 1a represents LL spectra at $B = 11\, T$ taken at the marked points in the topographic image shown in Fig. 1b. We confirm that $E_n$ exhibits a dependence on $B$ and $n$ typical for Dirac electrons$^{14,15}$. Moreover, the energy–momentum dispersion obtained by the scaling analysis$^{11}$ agrees quantitatively with that obtained by angle-resolved photoemission spectroscopy on crystals from the same source$^{20}$. These results guarantee that the obtained data faithfully represent intrinsic properties of the topological surface state (Supplementary Section 1.1). The potential landscape can be visualized by mapping the spatial variation of $E_n$. As LL$_0$ is independent of $B$ and is located at the Dirac-point energy, the $E_n$ map faithfully represents the potential landscape, albeit it is smeared over the size of the LL$_0$ wavefunction given by the magnetic length $l_B = \sqrt{|e|/|\mathbf{B}|}$. Here, $h$ is the Planck constant divided by $2\pi$ and $e$ is the elementary charge. At $11\, T$, $l_B$ is $\sim 7.7\, nm$. As shown in Fig. 1c, there is a well-defined potential minimum in the field of view which may be generated by subsurface charged defects (such as Se vacancies). There is a line-shaped protrusion in the lower right corner of Fig. 1b, but it hardly affects the potential map shown in Fig. 1c. Potential variations with a similar length scale were also observed in graphene$^{21}$ and doped topological insulators$^{22}$.

We find that the potential-gradient map (Fig. 1d) exhibits strong correlation with the map of the apparent width of the LL$_0$ peak (Fig. 1e), implying that the spatial variation of potential lifts the degeneracy of the LLs. This is clearly manifested in the individual tunnelling-conductance spectra shown in Fig. 1a. The LL$_0$ peaks are sharp and single peaks at the potential minimum (blue) and at the edge of the potential dip where the potential becomes almost flat (red). At the potential-gradient maximum (green), the LL$_0$ peak is not simply broadened but splits into multiple peaks which

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correspond to different quantum states as described later. Recently, similar splitting has also been observed in graphene\(^{33}\). Interestingly, the LL\(_1\) peak splits into two peaks even at the potential minimum. We will show below that this splitting of the LL\(_1\) peak is a direct consequence of the two-component nature.

Next we show the results of SI-STM around the potential minimum. Figure 2 shows a series of conductance maps at 11 T in the same field of view as in Fig. 1b–e. All the maps exhibit prominent ring-like structures, which are ascribed to the Landau orbits drifting along the equipotential lines\(^{17}\). The ring corresponding to the LL\(_0\) state emerges at the potential minimum and expands with increasing energy (Fig. 2a–c). With further increasing energy, the ring expands out of the field of view and another ring associated with the LL\(_1\) state evolves (Fig. 2d–f). Expansion of the ring is also observed in the LL\(_2\) state (Fig. 2g–i) and even higher LL\(_n\) states (not shown). The ring gets wider with increasing \(n\) and splits into two concentric rings for LL\(_n\), characterizing the internal structure of Landau orbits.
We further investigate the internal structure by analysing a series of conductance spectra taken along the line shown in Fig. 1b–e. As shown in Fig. 3a, the LDOS evolution shows the spatially dispersing Landau subbands. Corresponding to the peak splitting shown in Fig. 1a, 0 and 1 Landau subbands are broken at the potential-gradient maximum and at the potential minimum, respectively. The spatial evolutions of higher (n > 1) Landau subbands are smooth but each subband broadens and splits into two apparent branches at the intermediate region, which correspond to the two concentric rings in Fig. 2.

We examined the detailed LDOS distribution across the drifting Landau orbits by taking vertical line-cuts from Fig. 3a (Fig. 3b). As is already seen in Fig. 2, the Landau orbit gets wider with increasing n. This behaviour is common to both conventional and Dirac systems, because the quantum Larmor radii for n > 0 LLs, which characterize the widths of the Landau orbits, are given by \( l_B \sqrt{2n+1} \) and \( l_D \sqrt{2|n|} \) for conventional and Dirac systems, respectively (Supplementary Section 1.2).

A remarkable difference between the two systems appears in the internal structures. In the case of conventional systems, the LDOS variation across the drifting LL\(_n\) orbit exhibits \( n+1 \) peaks because the corresponding wavefunction contains \( n \) nodes\(^{25}\) (Supplementary Fig. 2). In contrast, in the case of the topological surface state of Bi\(_2\)Se\(_3\), the number of peaks never exceeds two, even for \( n > 1 \) LL states, as shown in Fig. 3b.

In the following, we show that our observations can be captured by model calculations and are direct consequences of the two-component wavefunction. We adopt a model Hamiltonian \( H = H_0 + V(r)\sigma_0 \), where \( H_0 \) represents the unperturbed Hamiltonian for two-dimensional Dirac electrons in \( B \) and \( V(r) \) is a circular-symmetric Coulomb potential generated by a subsurface charge\(^{23}\), \( \sigma_0 \) is the unit matrix.

It should be noted that the good quantum number here is the total angular momentum \( j_z \), which is a consequence of strong spin–orbit coupling. This is in contrast to the case of conventional systems, where the orbital angular momentum \( l_z \) specifies the quantum states\(^{25}\). Therefore, \( H \) is block diagonalized with respect to \( j_z \) and we can calculate the energy spectrum \( E_{n,j_z} \), the wavefunction \( \Psi_{n,j_z}(r) \), and the LDOS \( \Gamma(E, r) = \sum_{n,j_z} \Gamma((E - E_{n,j_z})^2 + \Gamma^2)|\Psi_{n,j_z}(r)|^2 \), assuming a Lorentzian broadening with a damping parameter \( \Gamma \). Details are given in the Supplementary Information.

Figure 4a shows an intensity plot of the calculated LDOS as a function of energy and \( |r| \), which reproduces the overall features of the experimental results shown in Fig. 3a. The discrete vertical ridges seen in the \( n = 0 \) Landau subband correspond to the different \( j_z \) states, which are degenerate for \( V(r) = 0 \). Once \( V(r) \) is turned on, this degeneracy is lifted because the Landau orbit with higher \( j_z \) drifts at larger \( |r| \), where the potential energy is higher.

Figure 4b depicts the calculated LDOS spectra at representative points, resembling the observed tunneling spectra shown in Fig. 1a. In particular, the splitting of the LL\(_{1}\) peak at the bottom of the potential is well captured. The physical picture of this splitting can be understood by looking into the nature of the wavefunction at \( r = 0 \). By inspecting the functional form of \( \Psi_{n,j_z}(r) \) given in the Supplementary Information, one finds that \( \Psi_{n,j_z}(r=0) \) consists of only two quantum states, with \( j_z = \pm 1/2 \) and \( j_z = \pm 1/2 \), which originate from the up-spin and down-spin components, respectively. Because these two states have different spatial extent, their energies are different; the LDOS peak splits accordingly. Thus, the splitting of the LL\(_{1}\) peak at \( r = 0 \) is a direct consequence of the two-component nature. The splitting should also occur for LL\(_{2}\) with \( n > 1 \), but its detection is much harder because the energy difference between \( j_z = \pm 1/2 \) states becomes smaller with increasing \( n \). Note that the LL\(_{0}\) peak does not split at \( r = 0 \) because only the down-spin component of \( \Psi_{n,j_z}(r=0) \) is non-zero. The relevance of this scenario is highlighted by looking at the spin-resolved LDOS at \( r = 0 \) (Fig. 4b).

The two-component nature also explains the absence of nodal structure in the LDOS distributions. The \( |r| \)-dependence of the calculated LDOS (Fig. 4c, thick black curves) exhibits only two peaks for \( n > 0 \), being in agreement with the experiment. We also plot the spin-resolved partial LDOS associated with the eigenstate at a given energy. Such a ‘dominating eigenstate’ mainly contributes to the total LDOS, albeit other states also participate if \( \Gamma \) is finite.
(Supplementary Section 1.5). Although the down-spin component (blue) has \( n \) nodes, as in the case of conventional systems, the number of nodes for the up-spin component (red) is \( n - 1 \). Therefore, the nodes for one component are always filled by the other, and two enhanced LDOS peaks are formed near the edges. These features are also expected in other two-dimensional Dirac systems such as graphene.

A unique feature of the topological surface states is that the potential variation not only affects the orbital motion but also induces non-trivial spin-magnetization textures through the strong spin-orbit coupling. Indeed, calculated spin-magnetization distributions shown in Fig. 4d–f exhibit energy-dependent cycloidal-helix-like patterns along the radial direction. A future spin-polarized STM experiment may detect these patterns directly. Such an emergence of spin-magnetization textures is not expected in graphene, where the Dirac electron nature is associated with the sublattice degrees of freedom. We anticipate that the combination of Landau quantization and a tailored potential landscape in the topological surface states may provide a novel ‘magnetoelastic’ control of spins, leading to intriguing spintronic and topological applications.

Methods

Bi\(_2\)Se\(_3\) crystals were prepared by the melt-growth technique. SI-STM experiments were performed at 1.5 K with a commercial low-temperature ultrahigh-vacuum STM (Uniosoku USM-1300) modified by ourselves. The clean and flat surface was obtained by in situ cleaving at \(-77\) K. After the cleaving, the sample was transferred quickly to the STM unit, which was kept below 10 K. Magnetic field was applied perpendicular to the cleaved surface. An electro-chemically etched tungsten wire was used as an STM tip, which was cleaned and characterized in situ with a field-ion microscope. Tunnelling spectra were taken with a software lock-in detector integrated in a commercial STM controller (Nanonis).

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Author contributions
Y-S.F. carried out the experiments and M.K. performed the theoretical modelling and calculations. Bi₂Se₃ single crystals were grown by K.I. and T.S. T.H. and H.T. supervised the project. Y-S.F., M.K. and T.H. designed the experiment, analysed the data and wrote the manuscript.

Additional information
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Competing financial interests
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