Backward Raman amplification in the Langmuir wavebreaking regime

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In plasma-based backward Raman amplifiers, the output pulse intensity increases with the input pump pulse intensity, as long as the Langmuir wave mediating energy transfer from the pump to the seed pulse remains intact. However, at high pump intensity, the Langmuir wave breaks, at which point the amplification efficiency may no longer increase with the pump intensity. Numerical simulations presented here, employing a 1D Vlasov-Maxwell code, show that, although the amplification efficiency remains high when the pump only mildly exceeds the wavebreaking threshold, the efficiency drops precipitously at larger pump intensities.

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I. INTRODUCTION

The largest laser powers are currently produced through chirped pulse amplification (CPA) technique1,2 (see also a recent review3). The power limit in CPA technique comes from the final material gratings needed to re-compress the amplified pulse (which was stretched before the amplification). Material gratings apparently cannot tolerate laser pulses so intense that the electron quiver energy reaches the material ionization energy. For laser wavelengths on the order of a micron, this limits the maximum laser intensity on gratings to a few TW/cm².

However, the maximum output in intensities reachable through backward Raman amplification (BRA) of laser pulses in plasma can, in principle, be nearly 10⁶ times larger.4 The BRA employs the resonant 3-wave decay of the pump laser pulse into the counter-propagating seed laser pulse and the Langmuir wave. The seed pulse captures substantial fraction of the pump energy and contracts reaching nearly relativistic intensities. Several other plasma-based mechanisms have also been proposed to compress laser pulses in a counter-propagating geometry. These mechanisms include Compton backscattering or, more recently, strongly-coupled Brillouin backscattering4–7 or possibly a combination of Raman and Brillouin backscattering8. However, at present, the BRA has enjoyed the most theoretical and experimental development, and appears to be the most promising for high intensity applications.

Inasmuch as the energy transfer in BRA is mediated by the Langmuir wave, the BRA efficiency can be significantly reduced by Langmuir wave breaking9–11, which occurs when the longitudinal quiver electron velocity exceeds the phase velocity of the Langmuir wave12. Apart from the Langmuir wave breaking, the BRA efficiency might be impeded by the amplified pulse filamentation and detuning due to the relativistic electron nonlinearity,13–16 parasitic Raman scattering of the pump and amplified pulses by plasma noise,17–20 generation of superluminous precursors of the amplified pulse,21 pulse scattering by plasma density inhomogeneities22, pulse depletion and plasma heating through inverse bremsstrahlung23–25, and resonant Langmuir wave Landau damping26,27. Taking into account these impediments to high efficiency, the regimes of the met robust efficiency can be identified28–30.

In the regimes in which the wavebreaking is not too strong, the BRA effect was demonstrated experimentally31,32. The experiments also indicated that the maximum BRA efficiency is achieved at pump intensities not exceeding by much the wavebreaking threshold31, in accordance with the theoretical expectations13.

Note that, apart from the issue of efficiency, there might be advantages to operating in the parameter regime prone to strong wavebreaking. For example, having larger laser-to-plasma frequency ratio (at which the Langmuir phase velocity is smaller) may reduce the parasitic Raman forward scattering of the amplified pulse33,34 while larger pump intensities might enable the amplified pulse to grow faster. The combination of these factors can incur strong wavebreaking.

Thus, it would be important if there were any possibility to increase the efficiency in strong wavebreaking regimes. This would be primarily important around the optical range. For UV and X-ray regimes,25,26 the wavebreaking intensities are already very high and not readily attainable at any Langmuir wave phase velocity exceeding a realistic thermal electron velocity, i.e. in the entire realistic range of the Langmuir wave existence. Recently in PIC simulations in the optical frequency range, high BRA efficiency was in fact reported in a very strong wavebreaking regime37. One of our purposes here was to confirm, in a different code, this optimistic prediction. However, while the efficiencies obtained here are in agreement with most of the efficiencies reported in the recent PIC simulations, they do not confirm the very high efficiency in the very strong wavebreaking regime.

Our paper explores the wavebreaking regimes numerically using the Vlasov-Maxwell (VM) code described below. First, we verify this code below wavebreaking. Then we apply this code to the pump pulse intensities exceeding the wavebreaking threshold. For mild wavebreaking regimes, where the pump intensities that exceed
the wavebreaking threshold by no more than a factor of just several, the VM code results are in agreement with both analytic calculations and previous PIC simulations. In this regime, highly efficient backward Raman amplification is still possible. For the strong wavebreaking regimes, we find that the BRA efficiency there basically agrees with both the analytical estimates of Ref. [1] and numerical results of Fig. 3a of Ref. [17] but is at variance with much higher BRA efficiency of Fig. 2a of Ref. [17]. In addition, we show that the BRA efficiency in the mild wavebreaking regime can be noticeably increased by increasing the input seed pulse intensity, while the BRA efficiency in the strong wavebreaking regime is basically not affected by increasing the input seed pulse intensity.

II. MODEL DESCRIPTION

To analyze the BRA wavebreaking regimes, we employ a one-dimensional (1D) relativistic Vlasov-Maxwell (VM) code. The non-relativistic version of this code can be found in [15,31]. The VM code is applicable to the BRA both below and above the wavebreaking threshold. In particular, below the threshold, this code covers the parameter range where the fluid description of the BRA is applicable, while, above the threshold, this code can properly handle kinetic effects important there. We solve full Maxwell equations, not using an envelope approximation for waves (even though it would much reduce the computational overhead and might be particularly useful for simulating multidimensional effects [32]), because the validity of the envelope approximations in the strong wavebreaking regime might still need to be verified independently.

The pump and seed pulses, counter-propagating the direction $\hat{z}$, are comprised of transverse electric and magnetic fields linearly polarized in $\hat{x}$ and $\hat{y}$ directions, respectively, $\vec{E} = E_x \hat{x}$ and $\vec{B} = B_y \hat{y}$. The seed pulse frequency $\omega_a$ is down-shifted from the pump frequency $\omega_p$ by the electron plasma frequency $\omega_p = \sqrt{4\pi n_e e^2/m_e}$, so that the Langmuir wave is resonantly excited, having the longitudinal electric field $\vec{E} = \hat{z} \vec{E}_z$. The fields are measured in units $m_e c\omega_e/e$, $m_e$ is the electron mass, $-e$ is the electron charge, $n_{e0}$ is the initial electron plasma concentration and $c$ is the speed of light in vacuum. The time $\tau$ is measured further in units $1/\omega_e$ and the distance $\xi$ is measured in units $c/\omega_e$. We also define the dimensionless frequencies $\bar{\omega}_a = \omega_a/\omega_e$ and $\bar{\omega}_p = \omega_p/\omega_e$, and the respective dimensionless wavenumbers $\bar{k}_a = \sqrt{\bar{\omega}_a^2 - 1}$ and $\bar{k}_p = \sqrt{\bar{\omega}_p^2 - 1}$. The resonant Langmuir wave then has the dimensionless wavenumber $\bar{k}_f = \bar{k}_a + \bar{k}_p$.

For the fast laser-plasma interaction of interest here, the slow ion motion can be neglected. The longitudinal electron distribution function $f$ is described by the one-dimensional Vlasov equation,

$$\frac{\partial f}{\partial \tau} + \frac{\bar{p}_z}{\gamma} \frac{\partial f}{\partial \xi} - (\bar{E}_z + \frac{\bar{p}_z}{\gamma} \bar{B}_y) \frac{\partial f}{\partial \bar{p}_z} = 0,$$  \hspace{1cm} (1)

where $\gamma = \sqrt{1 + P_z^2 + \bar{p}_z^2}$ is the Lorentz factor, $\bar{P}_z$ and $\bar{p}_z$ are the electron momentum components in the $\hat{z}$ and $\hat{\xi}$ directions, respectively, measured in units $m_e c$. The distribution function $f$ is measured in units $n_{e0}/m_e c$.

The electrostatic field $\vec{E}_z = -\partial \phi/\partial \xi$ is found by solving Poisson’s equation

$$\frac{\partial^2 \phi}{\partial \xi^2} = -[1 - \bar{n}_e(\xi, \tau)],$$  \hspace{1cm} (2)

where $\bar{n}_e(\xi, \tau) = \int f(\xi, \bar{p}_z, \tau) d\bar{p}_z$ is the electron concentration normalized to $n_{e0}$.

In this model, the electron motion in $\hat{x}$ direction is described by the fluid equation

$$\frac{\partial \bar{p}_x}{\partial \tau} = -\hat{E}_x,$$  \hspace{1cm} (3)

The electromagnetic waves are described by equations

$$(\frac{\partial}{\partial \xi} \pm \frac{\partial}{\partial \bar{p}_z}) \bar{E}_z = \int d\bar{p}_z \bar{P}_z \gamma f,$$  \hspace{1cm} (4)

where $\bar{E}_z = \bar{E}_x \pm \bar{B}_y$. The model Eqs. (1-4) conserves energy,

$$\frac{\partial}{\partial \tau}(W_{em} + W_{es} + W_k) = 0,$$  \hspace{1cm} (5)

where $W_{em} = \int d\xi (\bar{E}_x^2 + \bar{B}_y^2)/2$ is the electromagnetic energy, $W_{es} = \int d\xi \bar{E}_x \bar{B}_y/2$ is the electrostatic energy, and $W_k = \int d\xi \int d\bar{p}_z (\gamma - 1) f$ is the kinetic energy of the electrons. The model presented here is similar to that of Ref. [33]. In order to avoid electromagnetic wave reflections from boundaries, perfectly matching damping layers (PML) are inserted at both plasma edges. In order to avoid the Langmuir wave reflection, a Krook operator is added to the Vlasov equation that causes the electron distribution function $f$ to relax to the initial distribution $f_0$ in narrow boundary layers. To exclude extra spatial length from the numerical simulations, we solve the VM equations in the window around the seed pulse, using variables

$$\xi = \bar{\xi} + \tau, \quad \tau = \bar{t}.$$  \hspace{1cm}

Most of numerical examples will be presented below for the laser-to-plasma frequency ratio $\bar{\omega}_p = 20$ and the initial electron temperature $T_{e0} = 100 eV$. This temperature is much smaller than the energy of electron moving with the resonant Langmuir wave phase velocity, $v_{ph} = \omega_p/k_f \approx c/40$, which energy is $m_e c^2 v_{ph}^2/2 \approx 160 eV$. In such a plasma, the wavebreaking occurs when the amplitude of the longitudinal electron quiver velocity, $c E_L/(m_e \omega_e)$ exceeds $v_{ph}$. The amplitude of the Langmuir wave electric field $E_L$ at the wavebreaking threshold is then

$$E_L = \frac{m_e c \omega_e^2}{2e \omega_a}.$$  \hspace{1cm} (6)
The pump intensity at the Langmuir wavebreaking threshold can be evaluated as in [13]. Namely, the pump depleted energy is \( \tilde{\omega}_a \) (\( \approx 20 \)) times larger than the energy transferred to the Langmuir wave (since decay of one pump photon produces one Langmuir plasmon of \( \tilde{\omega}_a \) smaller energy). Therefore, to produce the Langmuir wavebreaking in initially quiet plasma, the input pump intensity \( I_0 \) should necessarily exceed the critical wavebreaking value \( I_{br} \),

\[
I_0 > I_{br} = \frac{c \tilde{\omega}_a}{16\pi} |E_L|^2 = \frac{m_e n_e c^3}{16 \tilde{\omega}_a}.
\] (7)

For the pump of wavelength \( \lambda_a = 0.8 \) \( \mu \)m and \( \tilde{\omega}_a = 20 \), the wavebreaking threshold is \( I_{br} = 33.6 \) TW/cm\(^2\). The respective amplitude of the electron quiver velocity in the pump field is \( \tilde{v}_{ea} = (2\tilde{\omega}_a)^{-3/2} = 0.004 \).

We will use the Gaussian input seed pulse of the form

\[
\tilde{E}_{seed}(\xi, \tau) = \tilde{v}_{eb, 0} \tilde{\omega}_b \exp[-(\xi - \xi_0)^2/2\Delta_b^2].
\] (8)

In most of the examples below the input seed pulse intensity is 10 PW/cm\(^2\), corresponding to \( \tilde{v}_{eb, 0} = 0.07 \), \( \Delta_b = 2\pi \) (i.e., the seed duration is one plasma period), and \( \xi_0 = 130 \).

The seed pulse is also characterized by the integrated seed amplitude \( U_m \),

\[
U_m = \sqrt{n_0 \tilde{\omega}_a \tilde{v}_{eb, 0} \Delta_b},
\] (9)

which, for the above parameters, is \( U_m = 3.5 \).

We will calculate the relative pump depletion, \( \eta \), far enough behind the seed, at \( \xi = 200 \),

\[
\eta = 1 - \frac{|\tilde{v}_{ea}(\xi = 200, \tau = 100)|^2}{|\tilde{v}_{ea, 0}|^2}
\] (10)

(here \( \tilde{v}_{ea} = \tilde{E}_a/\tilde{\omega}_a \) is the amplitude of the electron quiver velocity in the pump field, \( \tilde{E}_a \) is the electric field amplitude of the pump, and \( \tilde{v}_{ea, 0} \) is the input value of \( \tilde{v}_{ea} \)).

III. BRA BELOW THE WAVEBREAKING THRESHOLD

Consider first the well-studied case of BRA mediated by intact Langmuir wave. Let the input pump intensity be 4 times below the wavebreaking threshold (so that \( \tilde{v}_{ea, 0} = 0.5\tilde{v}_{ea} \)). The pump is rectangular, injected in the positive \( \xi \)-direction and the front is initially located at \( \xi = 100 \). In variables (\( \xi, \tau \)), the seed is not moving, while the pump propagates with the speed 2. Figure 1 shows the transverse and longitudinal electric fields \( \tilde{E}_x \) and \( \tilde{E}_z \) at \( \tau = 140 \). As seen, most of pump is depleted behind the seed pulse (\( \xi > 150 \)).

To separate electromagnetic fields of different waves, we use Fourier transformation. In the variables (\( \xi, \tau \)), the wavenumbers are the same as in (\( \tilde{z}, \tilde{t} \)), while frequencies of the pump, seed and Langmuir wave are, respectively, \( \tilde{\omega}_a = \tilde{\omega}_a + k_a\tilde{\omega}_b = \tilde{\omega}_a - \tilde{\omega}_b \) and \( \tilde{\omega}_f = \tilde{\omega}_a + k_f \). For \( \tilde{\omega}_a = 20 \), the frequencies and wave numbers are \( \tilde{\omega}_a \approx 40, k_a \approx 20,\)

\begin{figure}[h]
\centering
\includegraphics[width=0.8\textwidth]{fig1.png}
\caption{(Color online) The dimensionless transverse electric field, \( \tilde{E}_x \) (Fig. 1a), and longitudinal electric field, \( \tilde{E}_z \) (Fig. 1b), at the time \( \tau = 140 \) for the input pump intensity 4 times below the wavebreaking threshold and the input seed pulse intensity 10 PW/cm\(^2\).}
\end{figure}

\begin{figure}[h]
\centering
\includegraphics[width=0.8\textwidth]{fig2.png}
\caption{(Color online) The time-space Fourier-transformed transverse, \( \tilde{E}_x \) (Fig. 2a), and longitudinal, \( \tilde{E}_z \) (Fig. 2b), electric fields.}
\end{figure}

\begin{figure}[h]
\centering
\includegraphics[width=0.8\textwidth]{fig3.png}
\caption{(Color online) The envelope of space Fourier-transformed transverse electric field, \( \tilde{E}_x \), at the frequency \( \tilde{\omega} = 40 \) (Fig. 3a) and \( \tilde{\omega} = 0 \) (Fig. 3b). The envelope of space Fourier-transformed longitudinal electric field, \( \tilde{E}_z \), at the frequency \( \tilde{\omega} = 40 \) (Fig. 3c) and \( \tilde{\omega} = 0 \) (Fig. 3d).}
\end{figure}

\( \tilde{\omega}_b \approx 0, k_b \approx -19, \tilde{\omega}_f \approx 40, k_f \approx 39 \). Figure 2 shows the (\( \tilde{k}, \tilde{\omega} \)) Fourier-transformed fields \( \tilde{E}_x \) and \( \tilde{E}_z \). Two major spikes in the Fig. 2b, for the Fourier-transformed electric field \( \tilde{E}_x \), located at (\( \tilde{k}, \tilde{\omega} \)) = (20, 40) and (\( -20, -40 \)), correspond to the pump pulse, while two lesser spikes at (\( \tilde{k}, \tilde{\omega} \)) = (19, 0) and (\( -19, 0 \)) correspond...
to the seed pulse. Fig. 1b for the Fourier-transformed longitudinal field $\bar{E}_z$ contains 2 major spikes, located at $(\hat{k}, \hat{\omega}) = (39, 40)$ and $(\hat{k}, \hat{\omega}) = (-39, -40)$, corresponding to the resonant Langmuir wave that mediates BRA. There are also 2 lesser spikes, located at $(\hat{k}, \hat{\omega}) = (1, 0)$ and $(\hat{k}, \hat{\omega}) = (-1, 0)$, corresponding to the Langmuir wave that mediates forward Raman scattering of the seed pulse. Fig. 1b shows envelopes of the spatial Fourier-transformed fields $\bar{E}_E$ (Figs. 3a and b) and $\bar{E}_z$ (Figs. 3c and d) at frequencies $\hat{\omega} = 40$ (Figs. 3a and c) and 0 (Figs. 3b and d). These correspond to the pump (Figs. 3a), seed (Figs. 3b) and Langmuir waves mediating BRA (Figs. 3c) and forward Raman scattering of seed pulse (Figs. 3d).

The pump, seed and Langmuir wave envelopes can be restored from the $(\hat{k}, \hat{\omega})$ Fourier images using the Hilbert transform technique. These envelopes are shown in Fig. 1b. The pump behind the seed pulse is depleted by 90%. The incomplete pump depletion can be caused by the parasitic forward Raman scattering of the seed pulse and other deleterious processes. Fig. 1b shows the longitudinal electron momentum distribution function, $f$, at $\tau = 140$. For $\xi < 130$, no interaction occurs between the pump and the seed, and the distribution function stays close to the initial Maxwellian. For $\xi > 130$, the Langmuir wave is excited, and the distribution function is close to an oscillating Maxwellian, as it should be.

IV. BRA IN WA VEBREAKING REGIMES

We’ll now compare a mild wavebreaking regime, say with $\bar{v}_{ea}/\bar{v}_{br} = 1.5$, i.e., the input pump intensity 2.25 times above the wavebreaking threshold, to a strong wavebreaking regime with $\bar{v}_{ea}/\bar{v}_{br} = 5.5$, i.e., the input pump intensity 30 times above the wavebreaking threshold.

Figure 5 shows the transverse and longitudinal field amplitudes in these two regimes at $\tau = 90$. Despite the wavebreaking, the longitudinal field still appears to be larger at the larger pump intensity. Nevertheless, the pump depletion behind the seed pulse drops from 30% in the mild wavebreaking regime down to 9% in the strong wavebreaking regime.

Figure 6 shows the Fourier-transformed transverse electric field $\bar{E}_x$ in the mild wavebreaking regime, $\bar{v}_{ea}/\bar{v}_{br} = 1.5$, (Fig. 6a) and in the strong wavebreaking regime, $\bar{v}_{ea}/\bar{v}_{br} = 5.5$, (Fig. 6b).
FIG. 7. (Color online) The envelope of spatially Fourier-transformed transverse field $\bar{E}_x$ in the mild wavebreaking regime, $\bar{v}_{ea}/\bar{v}_{br} = 1.5$, at $\hat{\omega} = 40$ (Fig. 7a) and $\hat{\omega} = 0$ (Fig. 7b). The envelope of spatially Fourier-transformed transverse field $\bar{E}_x$ in the strong wavebreaking regime, $\bar{v}_{ea}/\bar{v}_{br} = 5.5$, at $\hat{\omega} = 40$ (Fig. 7c) and $\hat{\omega} = 0$ (Fig. 7d).

FIG. 8. (Color online) The time-space Fourier-transformed longitudinal field $\bar{E}_z$ in the mild, $\bar{v}_{ea}/\bar{v}_{br} = 1.5$, (Fig. 8a) and strong, $\bar{v}_{ea}/\bar{v}_{br} = 5.5$, (Fig. 8b) wavebreaking regimes.

FIG. 9. (Color online) The envelope of spatially Fourier-transformed longitudinal field $\bar{E}_z$ in the mild wavebreaking regime, $\bar{v}_{ea}/\bar{v}_{br} = 1.5$, at $\hat{\omega} = 40$ (Fig. 9a) and $\hat{\omega} = 0$ (Fig. 9b). The envelop of spatially Fourier-transformed longitudinal field $\bar{E}_z$ in the strong wavebreaking regime, $\bar{v}_{ea}/\bar{v}_{br} = 5.5$, at $\hat{\omega} = 40$ (Fig. 9c) and $\hat{\omega} = 0$ (Fig. 9d).

FIG. 10. (Color online) Envelopes of electron quiver velocities $\bar{v}_{ea}$, $\bar{v}_{eb}$, $\bar{v}_{ef}$, and $\bar{v}_{eg}$ in the fields of the pump pulse (dashed line), seed pulse (solid line), Langmuir wave mediating BRA (dotted line) and Langmuir wave mediating forward Raman scattering of the seed pulse (dash-dotted line) at $\tau = 90$ for $\bar{v}_{ea}/\bar{v}_{br} = 1.5$ (Fig. 10a) and $\bar{v}_{ea}/\bar{v}_{br} = 5.5$ (Fig. 10b).

FIG. 11. (Color online) The electron distribution function for the mild, $\bar{v}_{ea}/\bar{v}_{br} = 1.5$ (Figs. 11a and c), and strong, $\bar{v}_{ea}/\bar{v}_{br} = 5.5$ (Figs. 11b and d), wavebreaking regimes. Figs. 11c and d show the distribution snap-shuts at $\xi = 132$ (solid line) and $\xi = 150$ (dashed line). The effective electron temperatures at $\xi = 132$ and $\xi = 150$ are $T_e = 180$ eV and 470 eV, for the mild wavebreaking regime, and 620 eV and 870 eV, for the strong wavebreaking regime, respectively.

Finally, Fig. 12 shows the fraction of pump energy that is decayed (a), transferred to the seed (b), to electrostatic waves (c), and to plasma electrons (d), in the mild (solid curve) and strong (dashed curve) wavebreaking regimes.
As seen, the pump depletion is significantly larger in the mild wavebreaking regime.

V. DISCUSSION

The results obtained here are by and large in agreement with previously reported PIC simulations. However there are also significant discrepancies. In this section, the VM simulations presented here are compared both to previous PIC simulations as well as to theoretical expectations.

This comparison is made in Fig. 13 which shows the relative pump depletion, $\eta$, calculated using our VM code to the results of PIC code simulations, as well as to the analytical estimate for the strong wavebreaking regime $v_{ea}/v_{br} \gg 1$. The solid line is based on our VM simulations at the initial electron temperature $T_e = 10$ eV and input seed intensity 10 PW/cm$^2$. The dash-dotted line shows the analytical estimate, $\eta \sim (\bar{v}_{br}/\bar{v}_{ea})^2$. The dashed line is the same estimate with a smaller numerical coefficient, $\eta \sim 0.3 \times (\bar{v}_{br}/\bar{v}_{ea})^2$. The crosses at $v_{br}/v_{ea} = 0.61, 1.73,$ and 4.88 show the pump depletion calculated through PIC simulations and reported in Fig. 3a of Ref. 47. The cross at $v_{br}/v_{ea} = 5.5$ shows the pump depletion reported in Fig. 2a of the same Ref. 47. Finally, the diamonds show our VM results at larger input seed intensities, 40 PW/cm$^2$ (the diamond at $v_{ca}/v_{br} = 1.5$) and 100 PW/cm$^2$ (the diamond at $v_{ca}/v_{br} = 5.5$).

It can be seen that the PIC results presented in Fig. 3a of Ref. 47 agree reasonably well both with the analytical estimate of Ref. 4 and with our VM simulations. There is somewhat smaller pump depletion in Fig. 3a of Ref. 47. This might be due to premature backscattering of the pump by PIC noise in the simulations of Ref. 47. Note that numerical noise would act much like physical noise in inducing premature backscattering. Note also that, although not employed in these simulations, the premature backscattering of the pump by noise, whether physical or numerical noise, could, in principle, be suppressed by selective resonance detuning techniques. In any event, there is not large discrepancy between results presented in Fig. 3a of Ref. 47 and both our VM simulations and with the analytical estimate.

The large discrepancy occurs in the strong wavebreaking regime case shown in Fig. 2a of Ref. 47 where the pump intensity is 30 times higher than the wavebreaking threshold $(\bar{v}_{ca}/\bar{v}_{br} = 5.5)$. Here, the PIC results report a surprisingly high 35% BRA efficiency. This high efficiency disagrees with both our VM numerical simulations results and the analytical estimate of Ref. 4. The high efficiency also appear even to disagree with the efficiency shown in Fig. 3a of the same Ref. 47. In contrast to the 35% efficiency, the VM simulation, the analytical estimate, and Fig. 3a all give less than 10% pump depletion for such a regime.

The inset of Fig. 13 shows how the pump depletion depends on the input seed duration and amplitude in the mild wavebreaking regime, $v_{ca}/v_{br} = 1.5$. Results for the constant initial seed duration of one plasma period and few input seed amplitudes, marked in the inset of Fig. 13 by few different values of the parameter $\alpha = \bar{v}_{cb}/\bar{v}_{cb,0}$, are shown by the dashed line. Results for constant input seed amplitude, $\bar{v}_{cb} = 0.07$, and few input seed durations, marked by few values the parameter $\alpha = \Delta_0/\Delta_{0,0}$, are shown by the solid line. Results for constant seed inte-
grated amplitude $U_{in} = 3.5$ and few input seed durations are shown by the dash-dot line. Our results from the inset indicate that in the mild wavebreaking regime it is beneficial to choose high initial seed pulse intensity to obtain maximal BRA efficiency.

VI. SUMMARY

The wavebreaking BRA regime in strongly undercritical plasma ($\omega_d/\omega_e = 20$) was studied using a 1D Maxwell-Vlasov code. This code confirmed that efficient BRA is possible for the pump pulse intensities up to a few times larger than the wavebreaking threshold. However, for pump intensities exceeding by more than a factor of 10 the wavebreaking threshold, the amplification efficiency significantly decreases.

For example, for the pump intensity exceeding the wavebreaking threshold by a factor of 30, we only found possible a BRA efficiency of less than 10%. This low efficiency is consistent both with the analytical estimate of Ref. 3 and with Fig. 3a of Ref. 17. However, this low efficiency is at variance with Fig. 2a of the same Ref. 47 where the rather higher efficiency of 35% was reported. It remains of interest, but reserved for a future study, to consider why in fact this difference is so large.

A further important finding of this study is that, in the strong wavebreaking regime, in contrast to the mild wavebreaking regime, increasing the seed pulse intensity does not increase the BRA efficiency.

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