Fabricating THz spiral zone plate by high throughput femtosecond laser air filament direct writing

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The sixth-generation wireless communication will exploit the radio band with frequencies higher than 90 GHz, reaching terahertz (THz) band, to achieve huge signal bandwidths. However, the cost-effective fabrication methods of the key components in THz band, which can compromise large scale, high precision, and high efficiency, remain great challenges at present. In this work, we have developed a high throughput fabrication method based on the femtosecond laser filament direct writing. The ability of fabricating large-scale THz elements with high precision and fast speed has been demonstrated by fabricating 100 × 100 mm² spiral zone plates (SZPs), which can convert the Gaussian THz beam into vortex beam. The performance of the obtained THz vortex beam is in good agreement with the theoretical predictions. The fabrication method reported here has promising applications in fabricating various kinds of THz elements on substrates with both flat and curved surfaces.

At present, the fifth-generation (5G) wireless facility is being constructed with dramatic speed all over the world. The study of the sixth-generation (6G) wireless communication has also attracted extensive interests, which will use the radio band above 90 GHz, reaching terahertz (THz) band, to further extend the signal bandwidths. Highly directional electromagnetic wave is the suggested candidate to provide wireless links in 6G communication networks1,2. Therefore, the development of the advanced beam controlling technique is under urgent demand3,4.

Significant improvements on beam controlling has been made in optics, which mainly relies on the skillful design of micro-/nano-structuring elements5–7 and the state of art fabrication technology such as electron beam lithography8, extreme ultraviolet lithography9 and ion beam etching10. Fortunately, these advanced optical beam controlling methods and concepts can be directly transferred to the THz band. For example, the orbital angular momentum (OAM) of the vortex optical beam provides a new informational degree of freedom due to its infinite number of eigenstates characterized by the topological charges11. In the communication systems, OAM can greatly increase the volume of data transferring12,13. OAM has also aroused considerable attentions due to its applications in optical tweezers14,15 and quantum entanglement16,17. Generally, OAM modes can be generated by using spiral phase plates18,19, holographic diffraction gratings20,21, frequency selective metasurface22,23, and etc. However, compared with the research of OAM in optics, the investigations in the THz band are still lag behind.

Recently, using geometric phase elements made of space-variant birefringent slabs, Minasyan et al. produced the quasi-monochromatic THz vortex beam24. Wu et al. utilized a THz quarter wave plate, a spiral phase plate, and Teflon axicons to generate THz vortex Bessel beam25. Xie et al. employed a concentric ring metal grating and photo-generated carriers to form the THz vortex beam26. V-shaped metasurface antennas27 and photo patterned birefringence liquid crystal28 are also proposed to generate the THz vortex beam. It is worth emphasizing that for THz wave, due to its relatively long wavelength, strong diffraction occurs when it propagates in free space, leading to the large beam diameter. Therefore, large aperture component is required in order to facilitate the beam coupling. Besides, military and deep-space communications are often based on large size phased-array antenna, which also needs large aperture device29. However, the current fabrication techniques are always inefficient and cannot produce elements with large apertures, which greatly restricts the THz wave's practical applications.

In this paper, we develop a high throughput direct writing method using the femtosecond laser air filament, which can fabricate large scale THz elements with a lateral resolution of ~100 μm, i.e. ~l/30 for 0.1 THz wave. In the filamentation the pulsed laser beam propagates with a constant diameter (~100 μm) over a distance much longer than its coherence length. Further, the_viewer can be equipped with appropriate optics to produce the large scale THz elements with high precision and fast speed.

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longer than the Rayleigh length\(^30,31\), making the filament direct writing be able to fabricate structures on both flat and curved surfaces. Using the fabrication method proposed here, the large-size \((100 \times 100 \text{ mm}^2)\) THz SZPs with topological charges \(l = 0, 1\) and 3 are fabricated. The fabrication time for each element is \(~4\) min. The performance of the fabricated SZPs are characterized experimentally, which are in good agreement with the design schemes. The fabrication method proposed in this paper can fabricate structures on almost all kinds of materials using a single step. It can fabricate large area structures with a maximal writing speed of 1,200 mm\(^2\)/min. Furthermore, due to the diffraction-free property of the femtosecond laser filament, there is no rigid requirement for the focusing control. Therefore, compared with the commercial maskless laser lithography, the laser filament direct writing technique in this paper is more robust and easier to use, which is very suitable for fabricating large area THz elements.

**Methods**

**Sample preparation.** We used a quartz substrate of \(100 \times 100 \times 2\) mm\(^3\), soaked it in acetone, methanol and ultra-pure water successively. The quartz substrate was cleaned by ultrasonic washer for about 3 min, then washed with ultra-pure water and dried with nitrogen gun. The purpose of cleaning is to remove organic contaminants from the quartz surface to obtain a clean substrate. After cleaning, we used a vacuum coating machine to plate a silver film with a thickness of \(~60\) nm on the top of the quartz substrate. During the coating process, the sample is rotated by a speed of 20 r/min and an evaporation rate of 10 Å/s is achieved.

**Fabricating SZPs.** The experimental setup is schematically shown in Fig. 1a. A commercial Ti: sapphire femtosecond laser amplifier system (Legend elite, Coherent) produced 800 nm femtosecond laser pulses with a pulse width of 42 fs and a repetition rate of 2.5 kHz. An optical attenuator comprised of a half wave plate and a Glan prism was employed to adjust the laser energy. After reflected by a pair of high reflective mirrors M1 and M2, the pulse train was focused by a lens (\(f = 3,000\) mm) and delivered into a computer controlled two-dimensional galvanometer scanner. After reflected by a high reflective mirror M3, the femtosecond laser filament is produced around the geometrical focus of the focusing lens. During the fabrication process, the laser filament is scanned only in the region where the silver film needs to be removed. The laser pulse energy was fixed at 0.64 mJ in experiments and a 6-cm-long light filament appears near the focus of the focusing lens. The scanning speed of the filament in the XOY plane was set to be 200 mm/s during the experiments.

**Characterizing SZPs.** The experimental setup for characterizing the SZPs is shown in Fig. 1b. A 0.1 THz source S (IMPATT diodes, Terasense Inc.) employed to generate Gaussian CW THz waves with a beam waist diameter of \(~12\) mm (FWHM), a divergence angle of 9.3°, and an average power of 95 mW. The distance between the SZPs and the THz source is 300 mm. The transmitted THz beam after the SZPs was detected by a polarization sensitive THz point detector D (WR-10 ZBD, Virginia Diodes Inc.). In order to record the spatial distribution of the THz beam, the point detector is mounted on a 2D stepper motor driving translation stage and scans in the XOY plane with a scanning step of 1 mm. During the experiments, the THz detector is firstly rotated when it is centered on the optical axis until the signal value reaches the maximum, making sure that the polarization state of the THz wave is consistent with the polarization sensitive direction of the detector. Then, the zone plate is inserted between the source and the detector.
Results and discussions

THz vortex beams obtained by SZPs. Based on the radial Hilbert transform, in the polar coordinates \((r, \varphi)\), the phase function of the designed THz SZPs can be expressed as:\(^{32}\):

\[
F(r, \varphi) = \exp \left(j \frac{l \varphi - \pi r^2}{2} \right)
\]

(1)

where \(l\) denotes the topological charges, \(\lambda\) is the incident wavelength and \(f\) represents the focal length of the THz SZPs. The binary transmittance function of the THz SZPs can be written as:

\[
t(r, \varphi) = \begin{cases} 
1, \sin \left(\frac{l \varphi - \pi r^2}{2f} \right) \geq 0 \\
0, \sin \left(\frac{l \varphi - \pi r^2}{2f} \right) < 0
\end{cases}
\]

(2)

The SZPs’ patterns with different topological charges \((l = 0, 1, 3)\) are designed by Eq. \((2)^{32}\). The designed patterns are loaded to the software used to control the galvanometer, and finally the SZPs are fabricated by scanning femtosecond laser filament via the galvanometer. Figure 2a shows the optical image of the fabricated SZP with the topological charge \(l = 0\) and a focal length \(f = 50\) mm. The performance of this SZP was characterized using the setup in Fig. 1b. According to the Gaussian imaging formula, the image plane of the THz source is 60 mm behind the SZP. The intensity distribution of the THz beam was measured at three different positions in the vicinity of the image plane as is shown in Fig. 2b. The three positions are respectively corresponding to \(d' = 50\) mm, 60 mm and 70 mm (see Fig. 2b). The measured intensity distributions are shown in Fig. 2c,e. The
measured radial intensity profile at the image plane (P2) is presented as the solid curve in Fig. 2f, which agrees well with the simulation result indicated by the dotted line. The THz beam's focal spot has a diameter of 3.3 mm (Full width at half maximum, FWHM) at \(d' = 60\) mm, which coincides with the design scheme.

The THz SZPs with topological charges of 1 and 3 were fabricated and the optical images are respectively shown in Fig. 3a,b. Using Kirchhoff diffraction formula, the intensity and phase distribution of THz beam at the image plane of the designed SZPs can be calculated. The calculated results are presented in Fig. 3c,f. The measured THz beam intensity distributions at the image plane of SZPs with \(l = 1\) and 3 are respectively shown in Fig. 3g,h, which agree well with the calculation results.

It should be noted that the quartz substrate is not damaged after the removal of the silver film by the laser filament, because the laser fluence at the target surface is calculated to be 2.1 J/cm\(^2\) (the product of the clamping intensity \(5 \times 10^{13}\) and the pulse duration 42 fs) lower than the quartz damage threshold of 3 J/cm\(^2\). Furthermore, except for the quartz substrate, sapphire and diamond with high THz transmittance are both potential substrates for THz elements, which cannot be damaged by femtosecond laser filament due to their high damage thresholds.

**Spatial resolution of the direct writing system.** The spatial resolution of the femtosecond laser filament direct writing system determines the performance of the fabricated THz elements, so it should be inves-
tigated in detail. Figure 4a shows the optical image of the femtosecond laser filament used in our experiments. The length of the filament is about 6 cm. Although the maximal fabrication range in the XOY plane is calculated to be $1.194 \times 1.194 \, \text{m}^2$ using the geometries in Fig. 4b and assuming an axially uniform filament, the maximal fabrication range demonstrated experimentally is only $200 \times 200 \, \text{mm}^2$ due to the limited size of the mirror M3 in Fig. 1a. To investigate the spatial resolution of the fabrication system, the resolution chart (USAF-1951) array shown in Fig. 5a was directly written onto the surface of an aluminum foil sample ($200 \times 200 \times 0.3 \, \text{mm}^3$) and the fabrication result is shown in Fig. 5b. The zoom-in picture of the fabricated resolution chart in the periphery of the fabrication range is shown in Fig. 5c. It is seen that no defocus induced resolution loss appears in this image. By measuring the minimum feature size that can be achieved in each resolution chart, the spatial distribution of the fabrication resolution on the whole sample surface can be obtained, which is shown in Fig. 5d. The mean resolution and its standard deviation of the direct writing system are $93.9 \, \text{μm}$ (about $\lambda_{\text{THz}}/33$) and $16.6 \, \text{μm}$ respectively. The ~100 μm resolution is consistent with the diameter of the filament which can be measured by a thermal paper. The thermal paper is inserted perpendicular to the filament and the cross-sectional filament intensity pattern is recorded, which is shown in Fig. 4c. The diameter of the laser filament could be adjusted by controlling the focal length of the focusing lens, the laser peak power and the ambient air pressure. For example, by simultaneously controlling the focal condition and laser peak power, the filament diameter can be adjusted in the range of 30–100 μm. By increasing the air pressure from 1 to 4 atm, the filament diameter can be reduced by 50%38. Therefore, the laser filament with a diameter of 15 μm is expected by simultaneously modulating the focal condition, the laser peak power and the air pressure. As a consequence, the fabrication resolution of 15 μm may be achieved and 6G elements working at 0.6 THz with similar performance to those in our experiments may be fabricated by the method proposed in this paper.

Conclusions

In this paper, we propose a high throughput fabrication method based on the laser induced filamentation for the fast fabrication (~ 4 min) of large-size (100 × 100 mm²) THz SZPs with topological charges $l = 0, 1$ and 3. The intensity distribution of the THz beam in the image plane ($d' = 60 \, \text{mm}$) of the fabricated SZPs is measured which agrees well with the designed distributions. The maximal element size fabricated by our system is $200 \times 200 \, \text{mm}^2$. Meanwhile, the galvanometer scanner used in our experiments offers a fast fabrication speed (200 mm/s) and the fabrication of one SZP sample takes ~ 4 min.

By directly writing the standard resolution test chart (USAF-1951) array on a large-size aluminum sample, the mean resolution ($93.9 \, \text{μm}$) and its standard deviation ($16.6 \, \text{μm}$) of the laser filament direct writing system are determined. It is expected that by changing the laser power and focal condition, the fabrication resolution can be further improved which will be investigated in future researches. It concludes that the fast, high throughput, large scale laser filament direct writing method can find important applications in fabricating the large aperture elements, such as those used in the next generation wireless communications.

Data availability

The datasets generated and analyzed during the current study are available from the corresponding author on reasonable request.

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Author contributions
W.L. and N.Z conceived the study and designed the experiments. O.K. and L.L. performed the theoretical calculation. Z.Z., Z. D, Q.S., C.C. and Y.W. prepared and conducted the experiments, W.L., N.Z, Z.Z. and Z.D analyzed the data. All authors contribute to the writing of the manuscript.

Competing interests
The authors declare no competing interests.

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