Photodetachment and Doppler laser cooling of anionic molecules

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Abstract
We propose to extend laser-cooling techniques, so far only achieved for neutral molecules, to molecular anions. A detailed computational study is performed for \( \text{C}_2^- \) molecules stored in Penning traps using GPU based Monte Carlo simulations. Two cooling schemes—Doppler laser cooling and photodetachment cooling—are investigated. The sympathetic cooling of antiprotons is studied for the Doppler cooling scheme, where it is shown that cooling of antiprotons to subKelvin temperatures could becomes feasible, with impacts on the field of antimatter physics. The presented cooling schemes also have applications for the generation of cold, negatively charged particle sources and for the sympathetic cooling of other molecular anions.

1. Introduction

Atomic and molecular anions are relevant in a variety of different fields starting from the chemistry of highly correlated systems [1], the studies of planetary atmospheres [2], negative superhalogens [3] to the interstellar medium [4, 5]. The study of the processes in which the anions are involved is currently hampered by their synthesis at ultracold temperatures. Up to now, temperatures of at best several Kelvin have been achieved via supersonic expansion of anionic gas followed by resistive, buffer gas or electron cooling in cryogenic environments [6–11]. The utilization of laser cooling techniques, routinely used for neutrals, positive ions and neutral molecules (SrF, YO, CaF) [12–14], could for the first time allow the investigation of anionic systems at subKelvin temperatures. In a broader perspective, cooling even a single anion species would enable one to cool any other negatively charged particles via sympathetic cooling including \( \text{e}^- \), atomic and molecular anions and antiprotons. The latter are relevant for anti-hydrogen (\( \text{H}^- \)) experiments, since even though first spectroscopic results on the 1S–2S transition of \( \text{H}^- \) have been recently obtained [15], their current sensitivity to CPT violations is not yet competitive with that obtained with antiprotons [16, 17] or positrons [18]. Further, measuring the gravitational interaction between matter and antimatter with similar precisions as has been accomplished for matter experiments [19, 20] requires full control of the external and internal state of \( \text{H}^- \) and temperatures below mK. More generally, the precision of future \( \text{H}^- \) experiments strongly correlates with the temperature at which \( \text{H}^- \) can be prepared. Current techniques that rely on forming \( \text{H}^- \) by interacting \( \text{p}^- \) and \( \text{e}^- \) which have been pre-cooled in a cryogenic Penning trap achieve \( \text{H}^- \) temperatures in the region of 10 K [15]. The creation of ultracold \( \text{H}^- \) via the resonant charge exchange of antiprotons with ortho-positronium (o-Ps) is potentially, limited only by the recoil limit of the constituents [21].

This goals of obtaining ultracold \( \text{H}^- \) has recently sparked theoretical and experimental investigations to use laser-cooled atomic anions like \( \text{Os}^- \) and \( \text{La}^- \) [10, 22–24]. As another approach to this yet-to-be-realized procedure, molecular anions are a potential candidate for laser cooling down to the mK regime and have been studied in [11]. In [25] a Sisyphus cooling scheme using optical dipole forces was investigated including the sympathetic cooling of other anions. Here, similarly to Doppler cooling, optical dipole force cooling relies on multiple lasers that repump the population of the coolant in a quasi closed cycle.

In this article, an easy-to-implement scheme relying only on two optical transitions is presented as photodetachment cooling. In this scheme, a selective fraction of \( \text{C}_2^- \) molecules with high kinetic energies can be
removed by two-stage laser induced photodetachment, hereby reducing the temperature of the remaining particles after reaching plasma equilibrium once again. While commonly applied for the spectroscopy of anionic systems and C2. The potential curves of the molecule were calculated using the empirical function proposed in [32, 37]. Furthermore, it has well suited branching ratios between $\text{B}^3\Sigma_u^+ \rightarrow A^3\Pi_u$ decay channel is forbidden [30–34]. In comparison to atomic La, molecular C2 has a similar dipole transition but exhibits no unwanted photodetachment, no hyperfine structure and can be produced at low sub-eV kinetic energies [35]. Figure 1(a) shows an overview of the electronic and vibrational level structure of C2 and C2. The potential curves of the molecule were calculated using the empirical function proposed in [36], using spectroscopic parameters from [32, 37]. The vibrational levels are based on constants from [37]. For C2 the curves where shifted by the electron affinity $EA = 3.269$. The rot–vib and electronic spectra of C2 were simulated using the program PGOPHER [38].

2. Sympathetic Doppler cooling of C2/\bar{p}

C2 can be produced from plasma discharge of acetylene with internal energies in the sub-eV range at densities of 1013 m−3 [35, 39]. After selection of C2 in a mass spectrometer, the anions can be trapped in a Penning trap. In sequence, \bar{p} can be trapped in the same Penning trap at a different axial position. Starting from typical experimental conditions that are achieved at CERN’s Antiproton Decelerator facility approximately 105 \bar{p} can be caught and initially electron-cooled to eV kinetic energies [15, 40–42]. The \bar{p} can then be mixed with the C2 and with priorly loaded e− using potential manipulations, similarly as demonstrated in the preparation of different charge-to-mass–ratio species plasmas [43, 44]. Using electron cooling after the mixing process and considering a 1 T Penning trap at 10 K, temperatures of the C2/\bar{p}/e− ensemble around 100 K can be realized within a few tens of seconds [45]. Subsequently, by lowering the axial trapping potential confining the particles allows for additional evaporative cooling and the preparation of the mixed plasma at about 10 K [46].

In the trap the $E \times B$ field causes an azimuthal drift of the particles about the magnetic field axis. At a same radius the difference in mass of the two species will result in a difference in centrifugal force and with that

![Figure 1](image-url)
rotation rate. Collisional drag gives rise to a separation of the particles with the lighter \( \bar{p} \) drifting inwards and the heavier \( C_2 \) outwards. In thermal equilibrium the rotation of the plasma is rigid at a frequency \( \omega_a \) [43]. In the limit of zero Debye length, the density \( n_j \) of species \( j \) is then determined by \( \omega_a \) as \( n_j = 2\pi e^2 m_j (\Omega_j - \omega_a)/\epsilon^2 \), with \( m_j \) and \( \Omega_j \) the respective mass and cyclotron frequency [43]. For the case of \( \Omega_j \gg \omega_a \), the plasma will evolve to a spheroidal shape with approximately equal densities and \( \omega_a = e n / (2\epsilon_0 B) \). Axially, the particles oscillate with a frequency \( \omega_{ax} = 2\pi \times \nu_{T,ax}/2l_p \) with \( \nu_{T,ax} = \sqrt{k_B T/m} \) the thermal velocity and trapping length \( l_p \).

In order to study the effect of sympathetic cooling, figure 2(a) shows a simulation of Doppler cooling a \( C_2/\bar{p} \) plasma confined in a 1 T Penning trap. The Coulomb particle–particle interaction and the trapping field is simulated for a total of 1848 \( C_2 \) and 200 \( \bar{p} \) with time steps that resolve the cyclotron motion of the \( \bar{p} \) including \( N \)-body space charge effects. To scale the simulation to experimentally typical particle numbers \( N_p \sim 10^5 \) with a particle ratio of \( N_{C2} \sim 10N_p \) and to investigate possible geometrical plasma effects the Coulomb interaction force between the particles is increased by a factor \( C_f = 5000 \) without affecting the particle-trap interaction. For this case, the simulation is shown in figure 2(c). The computation is performed on a GPU running on the mass parallel platform CUDA and the \( N \)-body algorithm described in [47]. A fifth order Dormand–Prince integrator is used to calculate the force equation at each time step [48].

To implement Doppler cooling in the simulation, the lasers are applied along the \( z \)-axis and parallel to the magnetic trapping field, that acts as a quantization axis. In this configuration only \( \Delta M = \pm 1 \) laser transitions are allowed, whereas spontaneous decays from the excited states can occur on \( \Delta M = 0, \pm 1 \) transitions. Figure 1(b) depicts the relevant vib–rot \( C_2 \) levels in the 1 T field together with the lasers for Doppler cooling. The transition strength probabilities of the excited \( [A, \nu' = 0, N' = 1] \) state to the \( A \) state vibrational levels are 96, 4, \( 2 \times 10^{-6} \) (percentage of the Franck–Condon); the natural linewidth of the excited state is \( \Gamma_{sp} = 2\pi \times 3.13 \text{ kHz} \) [30, 32–34, 37]. Two narrow-band lasers at 2.53 \( \mu \text{m} \) address the two \( [X, \nu'' = 0, N'' = 0, M'' = \pm \frac{1}{2}] \rightarrow [A, \nu' = 0, N' = 1, M' = \pm \frac{1}{2}] \) transition. The cooling lasers are red detuned from resonance by \( \Delta \nu \). In order to achieve a quasi closed transition cycle of the populations two additional 2.53 \( \mu \text{m} \) lasers repump the \( [X, \nu'' = 0, N'' = 2, J'' = 2.5, 1.5] \) manifolds with imprinted sideband structures at 63 MHz (The power ratios of the carrier, first and second order sideband are considered with a modulation index of \( 1.8 \text{ as } l_0 \approx 2J_1 \approx J_2 \)). Each repump laser then addresses four \( \Delta M = \pm 1 \) transitions. From each of the two excited \( A \) states there are six allowed \( \Delta M = 0, \pm 1 \) transitions back to \( X \) into the \( J'' = 1.5, 2.5 \) states and two transitions into the \( J'' = 0.5 \) states. In a similar way, a total of four additional repump lasers at 4.59 \( \mu \text{m} \) are required to address the \( [X, \nu'' = 1] \) ro-vib levels. In total 20 laser induced transitions and 32 spontaneous decays are to be considered for the quasi closed cycle.

In the limit of \( \Gamma_{sp} \ll \delta \nu \), assuming typical IR-DFB laser linewidths of a few MHz in the simulation, the average cooling force from the Doppler cooling transitions [49, 50] is calculated for each time step using Einstein’s rate equations [51]. In steady-state the population is then evenly distributed between all molecular substates. Thus, molecules resonant with the detuned Doppler lasers are selected in the force equation and experience a net cooling force \( F_i = I A_i / h k_i \) per time step, with \( k_i \) the wave vector of the respective cooling transition \( i \). Here, \( A_i \) is the Einstein coefficient of one of the two Doppler cooling transitions and \( I / s \) the fraction of the steady-state population in the excited state as \( l = 1 / \sum_j = 0.045 \), as inverse to the number of all levels \( j \) from figure 1(b). For the simulation, the
Doppler and repumper lasers are calculated with circular polarizations and linewidths of $\delta \nu = 1$ MHz and linear polarizations and linewidths of $\delta \nu = 3$ MHz, respectively. For all lasers a power of 3 mW and a waist of 1.5 mm is used. The resulting average cooling force leads to a cooling time on the order of several seconds per Kelvin. In order to simulate the plasma evolution over a wide temperature range within practically accessible simulation times the average cooling force used in the following simulations is increased by a factor of $10^3$.

The particles are initialized at a temperature of $\sim 10$ K and at a density of $n = 8 \times 10^{11} \text{ m}^{-3}$. For the case of $C_2$ in figure 2(a) cooling of the $C_2^+$ together with sympathetic cooling of $\bar{p}$ is seen to temperatures of $\sim 4$ mK after 50 ms. Without the factor $10^4$ increase in the cooling force and for the parameters used in figure 2, the average number of scattered photons then corresponds to $1.3 \times 10^8$, with the velocity removed per photon recoil from the two cooling transitions as $\Delta v_i = \frac{\hbar}{2m} R_p$. Due to the unpumped $[X, \nu' = 2]$ states, after Doppler cooling a total of 26% of the anions are then expected to end up in these excited vibrational states.

For the plots in figure 2, the temperature values are obtained from Boltzmannian fits of the velocity histograms in axial $z$ direction, pictured in figure 2(b) for $\bar{p}$ at three different times together with the corresponding radial plasma profiles in the $x$-$y$ plane. At $C_2^+$ temperatures of 1.3 mK the coupling parameter that describes the correlated system as $\Gamma = \frac{\kappa^2}{(4\pi \epsilon_0 a kT)}$ with the Wigner–Seitz radius $a = (3/4\pi n)^{1/3}$ approaches values of $\Gamma \sim 174$, where the first-order liquid-solid phase transition to a crystalline plasma state is expected. The crystallization process is visible in the formation of radial plasma patterns as a function of the plasma aspect ratios, density and magnetic field [52], which are precursors to the formation of bcc-lattice planes [43]. For the present trapping geometry two shells are exhibited with an outer plasma radius of $R_p = 0.2$ mm. No pronounced centrifugal separation of the two species is visible, with the separation length defined by $\lambda_{sp} = kT/(\pi m_{C_2} - m_{\bar{p}}) R_p$ reaching values of $R_p$ for temperatures of $T \sim 10$ mK [43]. In figure 2(c) using $C_p = 5000$ and leaving all other parameters identical the particles attain temperatures of 3 mK and 500 mK for $C_2^+$ and $\bar{p}$, respectively, after a simulated time of $\sim 50$ ms with the onset of a temperature difference at about 3 K. Introducing the Coulomb factor $C_2$ effectively scales the coupling parameter $\Gamma_2 = C_2^2/\Gamma$ with $a_2 = C_2^2/a$. At 3 K $\Gamma_2$ yields about 174, where the formation of three radial shells are visible for the present parameters. Here, with $\lambda_{sp} \ll R_p$ centrifugal separation of the two species starts to be visible at a simulated cooling time of 20 ms with the lighter $\bar{p}$ predominantly concentrated in the inner shell limiting the sympathetic cooling via viscous drag to the outer $C_2^+$. Further, by increasing $C_2$ close binary collisions dominate to produce equipartition of the axial and radial motions, where the equipartition rate becomes exponentially small with increasing $b/\Gamma$, the ratio of the distance of the closest approach $b = \frac{\kappa^2}{(4\pi \epsilon_0 a kT)}$ and the cyclotron radius $\Gamma = \frac{\hbar}{2m \nu_T}$ of the two species [53, 54]. This effect further contributes to the observed difference in final temperature between the $C_2^+$ and $\bar{p}$.

We have further checked an intermediate simulation using $C_2 = 100$ where the onset of the temperature difference occurs at about 0.2 K with the final temperatures of 30 mK for $\bar{p}$ and 10 mK for $C_2^+$ consistent with a crystallization and the $\Gamma_2$ scaling. The simulations shown in figure 2 indicate that for the typical parameters considered, sympathetic cooling of $\bar{p}$ using $C_2$ is expected to work over a large range of temperatures down to subKelvin. Further, the sympathetic cooling occurs within about 1 ms in agreement with [55] on time scale much faster than the effect of the amplified Doppler cooling. This still holds for the simulation including a Coulomb factor.

3. Photodetachment cooling of $C_2^-$

To cool species with multilevel structures such as $C_2^-$ using the Doppler scheme requires mastering a full set of lasers to absolute frequency precisions on the order of MHz. Additionally, for species faced with narrow dipole transitions cooling times of the order of minutes have to be considered against plasma heating rates in Penning traps [56]. As a different cooling method we shall now study photodetachment cooling relying on only two lasers. Here, a Doppler laser can, for example, be realized with a frequency-doubled Ti:sapphire laser system obeying energy conservation, $E_D = \hbar \nu / 2.53 \text{ mJ}$ (1 MHz, 3 mW) and a waist of 1 mm addresses the $\{X, \nu' = 0, N' = 0, M' = \frac{1}{2}\}$ ground state. By that a fraction of molecules in a velocity window resonant with the laser field is transferred to the excited state $\{A, \nu' = 0, N' = 1, M' = \frac{1}{2}\}$; for cooling the laser frequency is chosen to select molecules with high kinetic energy. From the excited $A$ state, a second laser at $\lambda_{pd}$ then transfers the population above the photodetachment threshold, $E_D$, splitting $C_2^-$ into neutral $C_2$ and photoelectrons, see figure 1(a).

In order not to address the ground states the energy of the photodetachment laser $E_{pd} = \hbar \nu / \lambda_{pd}$ must be $E_{pd} < E_A$. The corresponding total photodetachment cross section $\sigma_{pd}$ from the state $\{A, \nu' = 0\}$ for varying photon energy $E_{pd}$ can be calculated as the sum over the partial cross sections $\sigma_{pd}$ for all quantum numbers $i$ of the $C_2^-$ states obeying energy conservation, $\sigma_{pd}(E_{pd}) = \Sigma_i \sigma_{pd;i}$. $\sigma_{pd;i}$ is derived by Geltman for homonuclear diatomic anions in [59] and $P_{pd;i}$ is the relative weight of the transition given by the Franck–Condon factor. A calculation including the molecular potential energies shown in figure 1(a) results in a lower limit of $\sigma_{pd}/\text{cm}^2 = 3.5 \times 10^{-17}$ [60, 61]. The cross section for $E_{pd}$ close to the threshold $E_A - E_D$ is significantly lower reaching $\sigma_{pd}/\text{cm}^2 \sim 1 \times 10^{-19}$. The expected photodetachment rate is then given by $\Gamma_{pd} = \sigma_{pd} I/E_{pd}$ for a laser intensity $I$ and has to be seen in comparison to the total natural decay rate of the excited state of $\Gamma_{sp} = 19.7 \text{ ms}^{-1}$ [32, 33]. Experimentally $\Gamma_{pd} > \Gamma_{sp}$ can, for example, be realized with a frequency-doubled Ti:sapphire laser system.
enhanced in a low finesse cavity at 380 nm (3.26 eV) close to the EA threshold. While the neutral C$_2$ molecules will escape the trapping potential after photodetachment of C$_2^-$, the released photoelectrons will continue to Coulomb-interact with the plasma. The photoelectrons’ angular distribution hereby depends on the angular momentum of C$_2^-$. The distribution can be described by the Cooper–Zare model [62, 63] and for simplicity will be approximated by an isotropic character for the following simulation. The kinetic energy of the photoelectrons is dominated by the residual binding energy given by the difference between the combined photon energy and the photodetachment threshold, $E_{e^D} = E_{pD} - E_{A, eD}$, and can take values of $E_{e^D} < 0.47$ eV. Only the fraction of released electrons which have a kinetic energy projection along the trap axis smaller than the axial confinement potential of the space charge plasma will stay trapped. This can be expressed by the limit angle $\beta = \arccos \left( \sqrt{U/e^D} \right)$ that defines the fraction of trapped photoelectrons as $\eta = 1 - \int_0^{\beta} \sin(\phi) \, d\phi$. These electrons will thus continue to equilibrate with the plasma due to Coulomb collisions and their coupling to the black-body radiation of the environment.

The described processes are simulated in figure 3(a) for 1000 C$_2^-$ particles in a 1 T Penning trap for a photodetachment rate of $\Gamma_{pD} = 85$ ms$^{-1}$ and an axial confinement of $U = 20$ mV. Employing Einstein’s optical rate equations on all relevant transitions shown in figure 2(b), the pumping and photodetachment process is included using the Monte Carlo method. In the simulation, the plasma is first initialized at a density of $n = 5 \times 10^{12}$ m$^{-3}$ and $T = 120$ K, which ranges close to temperatures measured using electrostatic plasma modes [64]. The 2.53 μm laser is blue-detuned from resonance to address only the fraction of anions with a high kinetic energy before interacting with a light field at $\lambda_{pD} = 442$ nm. At this wavelength $E_{e^D} = 20$ meV and all $e^-$ are trapped, $\eta = 1$. By this, molecules with high kinetic are removed from the trapping fields. After reaching

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**Figure 3.** (a) Simulation of photodetachment cooling in a 1 T Penning trap at $C_f = 1$ and $E_{e^D} = 20$ meV, see text for detail. The temperature evolution of initially 1000 C$_2^-$ (blue) is simulated together with the created photoelectrons. The initial laser detuning of the 2.53 μm laser is set to 1σ of the initial Doppler profile width as $\Delta \nu = 116$ MHz and is linearly swept to $\Delta \nu = 84$ MHz. (b) Velocity histograms at three different times with the corresponding radial plasma profile of C$_2^-$ (blue) and $e^-$ (red). (c) Calculation of the C$_2^-$/e$^-$ temperature evolution caused by photoelectrons with energy $E_{e^D} = 0.46$ eV for C$_2^-$ (solid, blue) and $e^-$ (dashed, red) and $E_{e^D} = 20$ meV for C$_2^-$ (dashed–dotted, dark blue) and $e^-$ (dotted, dark red). $N_{C_2} / N_{e^D} = 1.5 \eta$ and initial $T_{C_2} = 30$ K.
equilibrium once again [65], the remaining $C_2^- / e^-$ plasma are left with a mean reduced temperature. This process is very similar to evaporative cooling as performed with neutral atoms [66]. The number of $C_2^-$ in the trap decreases until it reaches a saturation level after $\sim 0.35$ ms, which is determined by loss of $C_2^-$ in unpumped molecular states. The confidence intervals are obtained from Boltzmann fits to the particle velocity distribution shown in figure 3(b) together with the radial plasma profiles. The temperature evolution for longer time scales $> 0.35$ ms caused by the released photoelectrons is shown in figure 3(c) for $\lambda_{pd} = 442$ nm and for the case of $380$ nm ($E_{e^-} = 0.47$ eV, $\eta = 0.21$). Here a coupled rate equation calculation of the $C_2^- / e^-$ plasma is performed including synchrotron radiation [45] in the trapping field. The final parameters of the GPU simulation from figure 3(a) at $t = 0.34$ ms are used as input values for figure 3(c) as the particle number ratio and the initial temperature of $C_2^-$ and $e^-$. Here, the temperature of the $C_2^-$ initially follows similar behavior for different photodetachment conditions. After approximately 2–5 s the system reaches temperatures of 100–400 K for increasing $e^-$ energies before electron cooling dominates. From these two plots one infers that for the considered density, B field and initial $C_2^-$ temperature the photoelectron heating occurs on a time scale about 30 times longer than the photodetachment cooling. Thus, in the overall temperature dynamics a temperature minimum is seen after $\sim 0.35$ ms at 50 K and is found to be robust for different $E_{e^-}$. It is thus this difference of time scales of the competing processes which allows for the technique of photodetachment cooling. Measurements at cold temperature can be then performed in an experimental window of $\sim 100$ ms.

In figure 4 photodetachment cooling is studied for $C_2^-$ at 10 K after electron cooling to the liquid helium Penning trap environment [67]. At this temperature the cooling is initialized with identical trap and laser
parameters as in figure 3. The result of the Monte Carlo simulation using 1100 C$_2^-$ molecules is depicted in figure 4(a). The mean kinetic energy of all anions is calculated from the square of the mean velocities from the histograms shown in figure 4(b). A temperature reduction of a factor of $\sim 5.5$ is seen for a C$_2^-$ number decrease by a factor of 2.5 after $\sim 0.32$ ms. Figure 4(c) plots the thermalization of C$_2^-$ and photoelectrons for a longer time scale $>0.32$ ms using rate equations [45] for two different $E_{\text{vac}}$. A window of approximately 10 ms can be used to perform measurements on cold anions which is sufficient for spectroscopic analysis of C$_2^-$ of any sympathetically cooled negative species or pulsed antihydrogen formation [21].

4. Summary

A detailed computational study including all influencing trapping and optical parameters was performed using GPU aided simulations for laser cooling of C$_2^-$ anions and the sympathetic cooling of $\bar{p}$ stored in Penning traps. Photodetachment cooling is discussed for the first time as an accessible method to generate anions in the subKelvin regime. For the typical density and temperature range investigated, this scheme relies on a system of only two commercially available lasers and allows for an approximately 10 ms long time window at ultracold temperatures for experimental measurements. The time window is found to be robust for a wide range of photodetachment energies. Further it was shown, by investigating Doppler cooling, that C$_2^-$ could be a suitable sympathetic coolant for $\bar{p}$ in cryogenic environments enabling their preparation at lower temperatures than currently achieved. Additionally, starting photodetachment cooling at even lower energies, e.g. after Doppler cooling or using a trap at dilution refrigerator temperatures could potentially assist in the preparation of an ensemble of mK $\bar{p}$. This step would permit the resonant charge exchange formation of ultracold antihydrogen [21] (by employing available pulsed positronium sources [68]) and thus allows sensitive studies of CPT symmetries and of the WEP with neutral antimatter systems.

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References

[1] Jin D S and Ye J 2012 Chem. Rev. 112 4801–2
[2] Biermann K 2006 Nature 444 E6
[3] Freza S and Skurski P 2010 Chem. Phys. Lett. 487 19–23
[4] Li X and Paldus J 2006 Chem. Phys. Lett. 431 179–84
[5] Simons J 2008 J. Phys. Chem. A 112 6401–511
[6] Gerlich D 1995 Phys. Scr. T95 256
[7] Deiglmayer I, Goritz A, Best T, Weidemuller M and Wester R 2012 Phys. Rev. A 86 043438
[8] Kumar S S, Hauser D, Jindra R, Best T, Geppert W D, Millar T J and Wester R 2013 Astrophys. J. 776 25
[9] Gabriele G, Khabbaz A, Hall D S, Heimann C, Kalinowsky H and Jhe W 1999 Phys. Rev. Lett. 82 3198
[10] Jordan E, Cerchiari G, Fritzschke S and Kellerbauer A 2015 Phys. Rev. Lett. 115 113001
[11] Yzombard P, Hamamda M, Gerber S, Doser M and Comparat D 2015 Phys. Rev. Lett. 114 213001
[12] Shuman E S, Barry J F and Demille D 2010 Nature 467 820–3
[13] Hummon M T, Yeo M, Stuhl B K, Kolopy A L, Xia Y and Ye J 2013 Phys. Rev. Lett. 110 1–5
[14] Zhelyazkova V, Cournol A, Wall T E, Matsushima A, Hudson J J, Hinds E A, Tarbutt M R and Sauer B E 2014 Phys. Rev. A 89 2–6
[15] Ahmadi M 2017 Nature 541 506–10
[16] Ulmer S et al 2015 Nature 524 196–9
[17] DiSicacca J et al 2013 Phys. Rev. Lett. 110 130801
[18] Dehmelt H, Mittelman R, Van Dyck R S and Schwinberg P 1999 Phys. Rev. Lett. 83 4694–6
[19] Peters A, Chung K and Chu S 1999 Nature 400 849–52
[20] Muller H, Peters A and Chu S 2010 Nature 463 926–9
[21] Doser M et al 2012 Class. Quantum Grav. 29 184009
[22] Kellerbauer A and Walz J 2006 New J. Phys. 8 45
[23] Warring U, Amoretti M, Canali C, Fischer A, Heyne R, Meier J O, Morhard C and Kellerbauer A 2009 Phys. Rev. Lett. 102 043001
[24] Pan L and Beck D R 2010 Phys. Rev. A 82 014501
[25] Fesel J, Gerber S, Doser M and Comparat D 2017 Phys. Rev. A 96 031401
[26] Trippel S, Mikosch J, Berhane R, Otto R, Weidemüller M and Wester R 2006 Phys. Rev. Lett. 97 193003
[27] Kim J, Weichman M, Sjolander T, Neumark D, Klos J, Alexander M and Manolopoulos D 2015 Science 349 510
[28] Hauser D et al 2015 Nat. Phys. 11 467
[29] Crucellier A 1990 J. Phys. B: At. Mol. Opt. Phys. 23 3585–607
[30] Rosmus P and Werner H J 1984 J. Chem. Phys. 80 5085
[31] Mead R D, Hefer U, Schulz P A and Lineberger W C 1985 J. Chem. Phys. 82 1723
[32] Spirko T and Šedivcová V 2006 Mol. Phys. 104 1999
[33] Jones P L, Mead R D, Kehler T M and Rosner S D, Lineberger W C 1980 J. Chem. Phys. 73 4419
[34] Shan-Shan Y, Xiao-Hua Y, Ben-Xia L, Kakule K, Sheng-Hai W, Ying-Chun G, Yu-Yan L and Yang-Qin C 2003 Chin. Phys. 12 745
[35] Tulej M, Knopp G, Gerber T and Raci P 2010 J. Raman Spectrosc. 41 853–8
[36] Zavitzas A A 1991 J. Am. Chem. Soc. 113 4755–67
[37] Ervin M K and Lineberger W C 1991 J. Phys. Chem. 95 1167–77
[38] Western C M 2017 J. Quant. Spectrosc. Radiat. Transfer 186 221–42
[39] Rehfuss B D, Liu D J, Dinelli B M, Jagod M F, Ho W C and Oka T 1988 J. Chem. Phys. 89 129–37
[40] Gabrielse G et al 2008 Phys. Rev. Lett. 100 113001
[41] Amsler C and Ariga A 2016 J. Phys.: Conf. Ser. 755 011001
[42] Enomoto Y et al 2010 Phys. Rev. Lett. 105 1–4
[43] Dubin D H E and O’Neill T M 1999 Rev. Mod. Phys. 71 87
[44] Jelenkovic B, Newbury A, Bollinger J, Itano W and Mitchell T 2003 Phys. Rev. A 67 63406
[45] Rolston S L and Gabrielse G 1989 Hyperfine Interact. 44 233–45
[46] Andrenesen G B et al 2010 Phys. Rev. Lett. 105 1–5
[47] Nyland L, Harris M and Prins J F 2007 GPU Gems 3 677–96
[48] Gorp S V and Dupre P 2013 AIP Conf. Proc. 1521 300
[49] Wineland D J and Itano W M 1979 Phys. Rev. A 20 1521
[50] Eschner J, Schmidt-Kaler F and Blatt R 2003 J. Opt. Soc. Am. B 20 1003
[51] Hoppner R, Roldan E, Valcarril G J D and Optica D 2012 Am. J. Phys. 80 882
[52] Totuji H, Tsuruta K, Totuji C, Nakano K, Kamon K and Kishimoto T 1999 AIP Conf. Proc. 498 77–82
[53] Jensen M J, Hasegawa T, Bollinger J J and Dubin D H E 2005 Phys. Rev. Lett. 94 025001
[54] Dubin D H E 2005 Phys. Rev. Lett. 94 025002
[55] Anderberg F, Driscoll C F and Dubin D H E 2010 Phys. Plasmas 17 55702
[56] Andrenesen G et al 2007 Phys. Rev. Lett. 98 025002
[57] Blumberg W A M, Itano W M and Larson D J 1979 Phys. Rev. A 19 139–48
[58] Barrick J B and Yukich J N 2016 Phys. Rev. A 93 023431
[59] Geltman S 1958 Phys. Rev. 104 176–8
[60] Douguet N, Kokouline V and Greene C H 2008 Phys. Rev. A 77 064703
[61] Kokouline V 2016 private communication
[62] Sanov A 2014 Annu. Rev. Phys. Chem. 65 341–63
[63] Surber E, Babbs R and Sanov A 2003 J. Phys. Chem. A 107 8215–24
[64] Amoretti M et al 2005 Phys. Plasmas 10 3056–64
[65] Anderberg F, Dubin D H E, O’Neill T M and Driscoll C F 2009 Phys. Rev. Lett. 102 185001
[66] Petrich W, Anderson M H, Ensher J R and Cornell E A 1995 Phys. Rev. Lett. 74 5352
[67] Amole C et al 2012 Nature 483 43–43
[68] Mariuzzi S, Bettotti P and Brusa R S 2010 Phys. Rev. Lett. 104 243401