Impact of dark matter models on the EoR 21-cm signal bispectrum

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ABSTRACT
The nature of dark matter sets the timeline for the formation of first collapsed halos and thus affects the sources of reionization. Here, we consider two different models of dark matter: cold dark matter (CDM) and thermal warm dark matter (WDM), and study how they impact the epoch of reionization (EoR) and its 21-cm observables. Using a suite of simulations, we find that in the WDM scenarios, the structure formation on small scales gets suppressed resulting in a smaller number of low mass dark matter halos compared to the CDM scenario. Assuming that the efficiency of sources in producing ionizing photons remain the same, this leads to a lower number of total ionizing photons produced at any given cosmic time and thus in a delay in the reionization process. We also find visual differences in the neutral hydrogen (H\textsc{i}) topology and in 21-cm maps in case of the WDM compared to the CDM. However, differences in the 21-cm power spectra, at the same neutral fraction, are found to be small. Thus, we focus on the non-Gaussianity in the EoR 21-cm signal, quantified through its bispectrum. We find that the 21-cm bispectra (driven by the H\textsc{i} topology) are significantly different in WDM models when compared with CDM, even for same mass averaged neutral fractions. This establishes that the 21-cm bispectrum is a unique and promising way to differentiate between different dark matter models, and can be used to constrain the nature of the dark matter in the future EoR observations.

Key words: cosmology: dark ages, reionization, first stars, dark matter - methods: numerical

1 INTRODUCTION
Cosmology is the study of the evolutionary history of the Universe, and one crucial missing chapter in this history is the Cosmic Dawn and Epoch of Reionization. This was the period when the first sources of light in the Universe were formed, and these and subsequent population of sources emitted the high energy X-ray and UV radiation, which in turn heated up and reionized the intergalactic medium (see Barkana & Loeb 2001; Furlanetto et al. 2006, for reviews). This is the period in the cosmic history when the universe has witnessed the formation of the first bound structures. Thus, the CD-EoR has significant implications on the large scale structures that we see around us today.

After the cosmological recombination, the Universe went into the dark ages during which the density fluctuations in the matter distribution grew and, after reaching a threshold, the matter collapsed to make the first bound objects. The nature of dark matter sets the timeline and characteristics of these first bound objects, which were the hosts for the first sources of light, so it is essential to see the impact of different dark matter models on the observables from the Cosmic Dawn and EoR. Then, the natural question that arises is whether one can use the differences in these observables, estimated for different dark matter models, in order to constrain the nature of dark matter. The present observational probes that allows us to have a peak in this epoch are the absorption spectra of high redshift quasars (Loeb & Barkana 2001; White et al. 2003; Boera et al. 2019) and the Thompson scattering optical depth of the Cosmic Microwave Background Radiation photons (Kaplinghat et al. 2003; Komatsu et al. 2011). However, these indirect probes provides a very limited and weak constrains on the CD-EoR. The H\textsc{i} 21-cm line, which arises due to the hyperfine splitting of the ground state of the neutral hydrogen, is a direct and most promising probe to study this period. Motivated by this, a large number of radio interferometers, including the GMRT (Paciga et al. 2013), LOFAR (Mertens et al. 2020; Ghara et al. 2020), MWA (Barry et al. 2019; Li et al. 2019) and PAPER (Kolopanis et al. 2019) are attempting a statistical detection of this signal using the power spectrum statistic. In parallel, there is a complementary approach to detect the sky averaged global 21-cm signal from the CD-EoR using experiments e.g. the EDGES (Bowman et al. 2018), DARE (Burns et al. 2017),

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and SARAS (Singh et al. 2018). The next-generation interferometers like the SKA (Koopmans et al. 2015; Mellema et al. 2015) are expected to see a giant leap in sensitivity, which will enable them to make tomographic images of the H\(^+\) distribution across cosmic time.

The nature of the dark matter is mostly unknown to us. We can classify the dark matter into cold, warm, and hot categories based on the free streaming length scale of the dark matter particles (see Schneider 2012, and references therein). The ACDM cosmology is consistent with several observations at large scales, including the observations of Lyman-\(\alpha\) forest at small and medium scales, clusters and CMB anisotropies. However, some discrepancies between the theory and observations arise at small scales \(\lesssim 1.0\) Mpc. Some of these are labelled as the too-big-to-fail problem, the core-cusp problem, satellite abundance, and galaxy abundance in mini-voids (see Primack 2009; Weinberg et al. 2015; Bullock & Boylan-Kolchin 2017, for more details). These issues may be resolved either by invoking astrophysical baryonic processes or by assuming the dark matter to be warm instead of cold. Cosmology and especially structure formation and evolution can thereby be a good probe for studying such dark sectors (Schneider 2012; Viel et al. 2013).

Two potential candidates for the warm dark matter are sterile neutrinos and gravitinos, both of which require the extensions of the standard model of particle physics (Dodelson & Widrow 1994; Viel et al. 2005; Boyarsky et al. 2019). However, in this work, we consider a thermal relic to be the candidate for the WDM. Unlike sterile neutrinos, this candidate is probably less motivated but easier to simulate given the fact that its transfer function has been more studied by several authors, also in terms of non-linear structure formation. Sterile neutrinos are a more massive and slower form of neutrinos that do not interact via weak forces like the active neutrinos. Also, the detection of an unidentified emission line in the X-ray spectra of the Andromeda galaxy and Perseus galaxy cluster can be explained by the decay of sterile neutrino (Bulbul et al. 2014; Boyarsky et al. 2014). Several studies have constrained the WDM particle mass using galaxy luminosity function of high redshift galaxies and Lyman-\(\alpha\) forest data (Kennedy et al. 2014; Corasaniti et al. 2017; Dayal et al. 2017; Safarzadeh et al. 2018) and found a robust lower bound on the thermal dark matter particle mass to be \(\gtrsim 2\) keV. Recent Lyman-\(\alpha\) forest power spectrum analyses point to somewhat tighter limits \(>3.5\) keV at the 2\(\sigma\) C.L. (Iršić et al. 2017). However, for the purposes of the present work it is appropriate to investigate values of the thermal masses that are also in principle already ruled out by other observables.

In this work, we consider the standard CDM model and thermal warm dark matter (WDM) with masses of the thermal relic of 2 and 3 keV. Investigations of the structure formation processes, in the WDM scenario and especially at high redshifts have been performed by e.g. (Maio & Viel 2015) (and references therein). Recently, reionization has been studied in the warm dark matter models or extensions of the standard CDM scenario by several authors (Gao & Theuns 2007; Lovell et al. 2014; Sitrin et al. 2014; Dayal et al. 2017; Villanueva-Domingo et al. 2018; Das et al. 2018; Lapi & Danese 2015; Carucci et al. 2015, 2017). These studies have focused on the 21-cm power spectrum and found the differences in the 21-cm power spectrum to be significantly small between different models of the dark matter, and probably not large enough to be detectable by the first generation of radio interferometers.

However, the 21-cm power spectrum can provide a complete description of a signal only if it is a Gaussian random process in nature. Whereas, the EoR 21-cm signal is highly non-Gaussian, specifically during the intermediate and later stages of reionization (see also (Pillepich et al. 2007)). The power spectrum therefore can not capture this non-Gaussian feature of the signal. The effort to differentiate between different models of dark matters using the 21-cm power spectrum will not be optimal as it does not capture the non-Gaussian information present in the signal. To capture this evolving non-Gaussianity, one would need to use a higher order statistic, the bispectrum, which is the Fourier equivalent of the 3-point correlation function. Recently, the CD-EoR 21-bispectrum has been investigated using both analytical models and numerical simulations (Bharadwaj & Pandey 2005; Shimabukuro et al. 2016; Majumdar et al. 2018; Watson et al. 2018; Hutter et al. 2020). These authors have independently confirmed that the two major sources of non-Gaussianity in this signal are the matter density fluctuations and the neutral fraction fluctuations. In this work, we aim to quantify the differences in the observables of the CD-EoR 21-cm signal for different dark matter models. Through this analysis we would like to identify the optimal statistics that can be used to distinguish between different dark matter models and their signature on the CD-EoR 21-cm signal.

This article is organized as follows: In section 2, we briefly discuss the formation of structures in different dark matter models. In section 3, we concisely describe our semi-numerical approach to simulate the redshifted 21-cm signal and methods to estimate different statistics out of it. Section 4 describes our results. In section 5, we summarize our findings.

Throughout this work, we have used the values of cosmological parameters as \(\Omega_m = 0.308, \Omega_b = 0.048, \Omega_{\Lambda} = 0.692, h = 0.678\) and \(\sigma_8 = 0.829\) (Planck Collaboration et al. 2016).

## 2 SIMULATING THE STRUCTURE FORMATION FOR DIFFERENT DARK MATTER MODELS

The dark matter can be classified into three categories, based on their characteristics, they are - cold, warm, and hot. This classification is done according to the free streaming scale of the dark matter particles (Bode et al. 2001; Abazajian et al. 2001; Schneider et al. 2013). In the early Universe, primordial density perturbations on the scales smaller than the free streaming length scale get damped. This is because the dark matter particles at these scales stream out from the overdense to the underdense regions, whereas the fluctuations on the scales larger than this scale remain unaffected.

The free streaming scale can be defined as the length traversed by a dark matter particle before the density perturbations start to grow significantly. It can be calculated as (Kolb & Turner 1990; Smith & Markovic 2011):

\[
\lambda_{fs} = \int_0^{t_{mre}} \frac{v(t)\, dt}{a(t)} \approx \int_0^{t_{mre}} \frac{c\, dt}{a(t)} + \int_{t_{mre}}^{t_{nr}} v(t)\, dt/a(t) \tag{1}
\]

where \(t_{mre}\) is the epoch of matter-radiation equality, and \(t_{nr}\) represents the onset of non-relativistic behavior of dark matter particles. Also, we have made use of the fact that in relativistic domain, \(v(t) \sim c\). In the non-relativistic regime as \(v(t) \sim a(t)^{-1}\) and during the radiation dominated era, \(a(t) \propto t^{1/2}\), so equation (1) leads to:

\[
\lambda_{fs} \approx \frac{2c}{a(t_{nr})} \left[1 + \log \left(\frac{a(t_{nr})}{a_{mre}}\right)\right] \tag{2}
\]

So, by increasing the time when the nature of dark matter particle became relativistic i.e. \(t_{nr}\), we can make the free streaming scale \(\lambda_{fs}\) larger. We can calculate the mass of a halo whose formation is
In the cold dark matter scenario, the dark matter particles become non-relativistic already at the time of decoupling \( t_{\text{dec}} \sim t_{\text{dec}} \), leading to a negligible free streaming length. Hence, it does not erase the initial perturbations on small scales, and we have a bottom-up scheme for the formation of structures in the CDM cosmology, with galaxies forming first and galaxy clusters later. Several dark matter simulations confirm this (Diemand & Moore 2011; Frenk & White 2012). However, this model is inconsistent with the observations on small scales.

In the warm dark matter scenario, the particles become non-relativistic later compared to the CDM model and the \( t_{\text{nr}} \) lies somewhere in between \( t_{\text{dec}} < t_{\text{nr}} < t_{\text{dec}} \). Thus, the free streaming scale of the dark matter particles in the WDM model is larger compared to the CDM model leading to suppressed mass perturbations at small scales. It results in a bottom-up structure formation at scales greater than \( \lambda_{\text{fs}} \) and a top-down structure formation at scales less than \( \lambda_{\text{fs}} \). Also, various simulations of warm dark matter models confirm this (Bode et al. 2001; Schneider et al. 2012; Viel et al. 2013).

We used GADGET 2.0 N-body simulations (Springel 2005) for dark matter for a volume of 50 h\(^{-1}\) com. Mpc\(^3\) with 1024\(^3\) dark matter particles (see Table 1). The gravitational softening is chosen to be 1/30 of the mean linear interparticle separation. The mass of each DM particle is \( 9.95 \times 10^6 \) \( \text{M}_\odot /h \), thereby DM haloes of \( 10^9 \) \( \text{M}_\odot /h \) are resolved with about 100 particles. Compared to other investigations of DM structure formation, this is more focussed on the small scales and the volume and resolution used here are ideal to probe the 21cm signal and the WDM induced effects. Initial conditions for WDM are generated according to the fitting formula presented in (Viel et al. 2005), with thermal velocities drawn from a Fermi-Dirac distribution. The simulations’ snapshots store the position and velocities of the dark matter particles at these predesignated redshifts. We, next use a Friends-of-Friend algorithm to identify the collapsed gravitationally bound objects (halos) in these dark matter fields.

Figure 1 shows the two-dimensional slices of the matter overdensity field over-plotted with the halo fields obtained through these simulations. This plot shows all dark matter models at \( z = 8 \), where one can observe some visual evidence of the damping of matter density fluctuations on small scales in the WDM scenarios. Also, note that the free streaming length \( \lambda_{\text{fs}} \) scales with the mass of the warm dark matter particle as \( \lambda_{\text{fs}} \propto (m_{\text{wdm}})^{-4/3} \). These scaling relations have been derived in (Schneider et al. 2012; Smith & Markovic 2011). So, the lighter the WDM particle, the larger the free streaming scale, and the suppression will be more pronounced in 2 keV WDM model compared to 3 keV WDM model. This feature can also be seen in Figure 1 if we compare the matter overdensity and the halo mass field in the two WDM models.

This suppression of density fluctuations at small scales will
reduce the number of low mass halos in the WDM scenarios. In Figure 2, we show the halo mass function obtained at three redshifts \( z = 10, 8, \) and 6 for all dark matter models. We observe that at any redshift, the number of low mass dark halos gets reduced in the WDM model if we compare it to the CDM model. Also, we observe that the suppression of low mass halos is more for 2 keV WDM model compared to the 3 keV WDM model because the lighter the WDM particle, the larger the free streaming scale, and the formation of a more massive halo will be suppressed [see Equation (3)]. However, the number of massive halos in the WDM model is very similar to the CDM model, as, above the free streaming scale, the structure formation proceeds similarly to the CDM model. We have also shown the theoretically predicted Sheth-Tormen halo mass function estimated using a top-hat filter for all the dark matter models, where the transfer function in WDM scenarios is computed following the approach of Viel et al. (2005); Schneider et al. (2013).

### 3 SIMULATING THE REDSHIFTED 21-CM SIGNAL FROM THE EOR

We have used the ReionYuga\(^1\) semi-numerical simulations to simulate the redshifted 21-cm signal (Majumdar et al. 2013; Majumdar et al. 2014; Mondal et al. 2017). This simulation method is somewhat similar to the methods followed by Furlanetto et al. (2004); Choudhury et al. (2009); Zahn et al. (2011); Mesinger et al. (2011). Steps that are involved in this method can be summarized as follows: (I) Generating the dark matter density field, (II) Identifying the position and mass of the collapsed structures, i.e., halos, in the dark matter field, (III) Assigning the ionizing photon production rates to these halos, (IV) Generating the ionization maps including the effect of redshift space distortions and (V) Converting these ionization maps into redshifted 21-cm brightness temperature field.

As discussed in Section 2, we have used GADGET 2.0 N-body simulations to accomplish steps I and II. For the purpose of this work, we next assumed that the hydrogen follows the simulated dark matter density field at these redshifts (Table 1). Further, as our reionization source model (step III), we assume that the number of ionizing photons produced by a halo is proportional to its mass (Choudhury et al. 2009; Majumdar et al. 2014):

\[
N_{\gamma}(M) = N_{\text{ion}} \frac{M}{m_{\text{HI}}},
\]

where \( m_{\text{HI}} \) is the mass of a hydrogen atom, \( M \) is the mass of the halo, and \( N_{\text{ion}} \) is a dimensionless free parameter, which may depend on various other degenerate reionization parameters including star-formation efficiency of a source, escape fraction of ionizing photons from these sources etc. We set \( N_{\text{ion}} = 23.21 \) to achieve \( \bar{x}_{\text{HI}} \approx 0.5 \) at \( z = 8 \) in the CDM model. This additionally ensures that for the CDM model, the CIB density in the halo does not exceed the average, \( \bar{x}_{\text{HI}} \approx 0.5 \). We also assume that there is a Thompson scattering optical depth that is consistent with the CMB observations.

Next, we perform the step IV, i.e., we produce the ionization map, using the \( H^1 \) density map and the ionizing photon density maps. We use an excursion-set based algorithm to produce the ionization map at the desired redshifts. In this formalism, we first map the hydrogen density and ionizing photon density fields on a coarser 128\(^3\) grid with grid spacing \( 0.07 \times 8 \) \( \text{Mpc} \). Next, to identify the ionized regions, we smooth both the \( H^1 \) and ionizing photon fields using spheres of radius \( R \) for \( R_{\text{min}} \leq R \leq R_{\text{max}} \). where \( R_{\text{min}} \) is the resolution of the simulation which is equal to the grid spacing and \( R_{\text{max}} \) is the mean free path of the ionizing photons which we determine from Songaila & Cowie (2010). For any grid point \( x \), if the averaged ionizing photon density \( \langle n_{\gamma}(x) \rangle_R \) is higher than the density of \( H^1 \) at that point \( \langle n_{\text{HI}}(x) \rangle_R \) for any \( R \), then we flag that grid point as being ionized. The points which do not meet this criteria, we assign an ionization fraction \( x_{\text{HI}}(x) = \langle n_{\gamma}(x) \rangle_R / \langle n_{\text{HI}}(x) \rangle_R \) to them. This is repeated for all grid points in the simulation volume and for all \( R \) within the allowed range and the ionization map is produced. This ionization is then converted into the 21-cm \( H^1 \) brightness temperature map (step V) following the Equation (5).

\[
\delta T_b = 27 \, x_{\text{HI}} \, (1 + \delta_b) \left( \frac{\Theta_b \, h^2}{0.023} \right) \left( \frac{0.15 \, 1 + z}{\Omega_m \, h^2 \, 10} \right)^{1/2} \times \left( \frac{T_s - T_F}{T_b} \right) \tag{5}
\]

where \( x_{\text{HI}} \) is the neutral hydrogen fraction, \( \delta_b \) is the fractional baryon overdensity, \( T_s \) and \( T_F \) are the spin temperature and the CMB temperature respectively. In this work, we assume that during reionization the IGM is substantially heated above the CMB.

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\(^1\) https://github.com/rajeshmondal18/ReionYuga

![Figure 3. Reionization history for CDM (Red), 3 keV WDM (Green) and 2 keV WDM (Blue) with the variation of mass averaged neutral fraction \( \bar{x}_{\text{HI}} \).](image)

Table 1. This tabulates the redshift \( z \) and corresponding mass averaged neutral fraction \( \bar{x}_{\text{HI}} \) for all the dark matter models, for which we have simulated the 21-cm signal.

| Redshift \( z \) | \( \bar{x}_{\text{HI}} \) (CDM) | \( \bar{x}_{\text{HI}} \) (3 keV WDM) | \( \bar{x}_{\text{HI}} \) (2 keV WDM) |
|-----------------|----------------|----------------|----------------|
| 10.00           | 0.84           | 0.90           | 0.94           |
| 9.25            | 0.75           | 0.84           | 0.90           |
| 9.00            | 0.71           | 0.81           | 0.88           |
| 8.65            | 0.64           | 0.77           | 0.84           |
| 8.00            | 0.47           | 0.64           | 0.75           |
| 7.50            | 0.30           | 0.51           | 0.64           |
| 7.00            | 0.11           | 0.34           | 0.51           |
| 6.00            | 0.00           | 0.03           | 0.13           |
3.1 Statistics of the simulated EoR 21-cm signal

Visibilities, which are the Fourier transform of the sky brightness temperature, are the basic observables in any radio interferometric observation. This is one of the major reasons why most of the efforts to quantify the 21-cm signal is focused towards using various Fourier statistics. For this work we consider an idealistic scenario where there is no foregrounds emission or noise present in the data and the visibilities contain only the Fourier transform of the signal brightness temperature $\Delta T_b(\mathbf{k})$. The two Fourier statistics that are in our focus for this work are power spectrum and bispectrum.

3.1.1 21-cm power spectrum

One can define the 21-cm power spectrum as:

$$\langle \Delta T_b(\mathbf{k}) \Delta T_b^*(\mathbf{k}') \rangle = (2\pi)^3 \delta^3(\mathbf{k} - \mathbf{k}') P(k) \quad (6)$$

where $\delta^3(\mathbf{k} - \mathbf{k}')$ is the Dirac delta function, defined as:

$$\delta^3(\mathbf{k} - \mathbf{k}') = \begin{cases} 1, & \text{if } \mathbf{k} = \mathbf{k}' \\ 0, & \text{otherwise} \end{cases} \quad (7)$$

To estimate the 21-cm power spectrum, we divide the entire $k$ range (determined by the smallest and largest length scales probed by our simulation) into 10 equispaced logarithmic bins. Next, we Fourier transform the simulated 21-cm brightness temperature volume and use Equation (6) to estimate the power spectrum.

3.1.2 21-cm bispectrum

Similar to the power spectrum the bispectrum can be defined as:

$$\langle \delta_k(\mathbf{k}_1) \delta_k(\mathbf{k}_2) \delta_k(\mathbf{k}_3) \rangle = V \delta^K_{k_1+k_2+k_3} b_3(\mathbf{k}_1, \mathbf{k}_2, \mathbf{k}_3) \quad (8)$$

where $\delta^K_{k_1+k_2+k_3}$ is the Kronecker Delta function that ensures that the three $\mathbf{k}$ modes involved form a closed triangle (see top panel of Figure 4) i.e.,

$$\delta^K_{k_1+k_2+k_3} = \begin{cases} 1, & \text{if } (\mathbf{k}_1 + \mathbf{k}_2 + \mathbf{k}_3) = 0 \\ 0, & \text{otherwise} \end{cases} \quad (9)$$

Following the definition of the bispectrum one can define a binned estimator for this statistic as:

$$\hat{B}(k_1, k_2, k_3) = \frac{1}{N V} \sum_{(k_1+k_2+k_3)=0} \Delta_3(k_1) \Delta_3(k_2) \Delta_3(k_3) \quad (10)$$

where the total number of triangles that belong to the $n^{th}$ triangle configuration bin is $N$, and $V$ is the simulation volume.

To estimate the bispectra from the simulated signal we follow the algorithm of Majumdar et al. (2018). In their algorithm Majumdar et al. (2018) have parametrized the triangle configurations using two independent parameters:

1. The ratio between the length of the two arms of a $\mathbf{k}$ triangle

$$\frac{k_2}{k_1} = n \quad (11)$$

2. The cosine of the angle between these two arms

$$\cos \theta = \frac{k_1 - k_2}{k_1 k_2} \quad (12)$$

This parametrization helps in reducing the overall computation time for bispectrum estimation.

For a comprehensive understanding of the 21-cm bispectra, we need to estimate the bispectra for all possible unique triangle configurations. We follow the prescription of Bharadwaj et al. (2020).
that allows us to identify all possible unique triangles using the two parameters defined in Equations (11) and (12) and by imposing the additional condition on the triangle parameter space i.e.:

$$k_1 \geq k_2 \geq k_3 \implies \frac{k_2}{k_1} \cos \theta \geq 0.5$$  (13)

Figure 4 shows the unique triangle configurations in the $n - \cos \theta$ parameter space.

4 RESULTS

4.1 Reionization history and 21-cm topology

The differences in the dark matter models have two prominent impact on the 21-cm signal from the EoR. One of them is the delay in the global reionization process, which is evident from the $\bar{x}_{H_i} - z$ and $\bar{T}_b - z$ curves for different dark matter models in Figure 3. The reionization starts and finishes later in the WDM scenarios compared to the CDM scenario. This is a clear signature of the differences in the structure formation history in different scenarios (shown through the halo mass functions in Figure 2). The halo mass functions plotted in Figure 2 reveals that the low mass halos cumulatively are the dominant sources of ionizing photons (when we assume all halos are equally efficient in producing ionizing photons) at any redshift for all dark matter models considered here. In case of the warm dark matter models, the low mass end of the halo mass function gets suppressed compared to the cold dark matter scenario, which results in an overall decrease in the total number of ionizing photons produced at any redshift. This overall reduction in the total number of ionizing photon produced at any redshift leads to a delay in the reionization process for the WDM models compared to the CDM one. The suppression of the low mass end of the halo mass function is more pronounced in the case of the 2 keV WDM model compared to the 3 keV WDM model, which leads to an even longer delay in the reionization process in case of the 2 keV WDM model.

The other prominent impact that the differences in the dark matter models on the reionization process have is the differences in the $H_i$ 21-cm brightness temperature topology. This is also caused by the different level of suppression of the low mass end of the halo mass function in different dark matter models. Figure 5 shows two-
dimensional slices of the $H_\text{I}$ 21-cm brightness temperature maps at three different redshifts: $z = 9, 8$ and 7 for all dark matter models. In these figures, a clear difference in the size and location of the ionized regions is visible in different models of dark matter. However, it is important to note that even if the 21-cm maps are shown at the same redshifts, they are not at the same state of reionization for different models of the dark matter. One may ask the question how much of this observed difference in 21-cm topology is due to the delay in reionization history. To address this, Das et al. (2018) have tuned the ionizing photon production efficiency (i.e. the parameter $N_{\text{ion}}$ in our simulations) of halos in different dark matter models to get the same global neutral fraction at the same redshifts for all dark matter models. With this modification in their simulations, they still observed significant differences in the 21-cm topology and its Fourier statistics for different dark matter scenarios. However, one should note that, changing the $N_{\text{ion}}$ in different scenarios effectively means changing the reionization model all together. Therefore, for the main analysis and results in this paper we keep the value of $N_{\text{ion}}$ same for all dark matter scenarios. We briefly discuss the impact of changing the $N_{\text{ion}}$ (to get the same reionization history) for different dark matter models on the 21-cm statistics (observable) in Appendix A.

4.2 21-cm Power Spectrum

We next focus our attention to the statistic that one would use to detect the EoR 21-cm signal using radio interferometers, i.e. the power spectrum. The power spectrum quantifies the amplitude of fluctuations in the signal at different length scales. The top panel of Figure 6 shows the power spectrum in all three dark matter scenarios (represented using three different line styles) at three different redshifts (represented using three different line colours). The evolution of the power spectra with redshift for a specific dark matter model demonstrated in Figure 6 follows the behaviour of an inside-out reionization (Choudhury et al. 2009; Mesinger et al. 2011; Zahn et al. 2011; Majumdar et al. 2014; Mondal et al. 2017), i.e. ionization starts at the highest density regions (where the ionizing sources are) in the IGM and then it gradually makes it’s way to the low density regions. The kind of inside-out reionization makes power at the large scales (small $k$ modes) grow in amplitude as reionization progresses and reach its peak at $\bar{x}_{\text{HI}} = 0.5$ and then go down in amplitude. The top panel of Figure 6 clearly shows that the difference in the 21-cm power spectra for different dark matter models is quite large (by even few orders of magnitude in certain $k$ modes), when they are compared at the same redshifts. However, even if these power spectra are at the same redshifts, they are from different stages of reionization for different dark matter models. To get a better idea of how a dark matter model impacts the reionization process it is more reasonable to compare the 21-cm statistics at the same stage of reionization (determined by the $\bar{x}_{\text{HI}}$ value) in different dark matter models.

4.2.1 Difference in 21-cm power spectrum between different models at same mass averaged neutral fraction

The amplitude of the redshifted 21-cm power spectrum during the EoR is determined mainly by the fluctuations in the neutral fraction ($\bar{x}_{\text{HI}}$) field. This is why it is more logical to compare the EoR 21-cm power spectra from different dark matter models at the same stages of reionization (i.e. approximately for the same values of $\bar{x}_{\text{HI}}$). Here the expectation is, when compared for the same values of $\bar{x}_{\text{HI}}$, the differences in $P(k)$ will be mainly due to the differences in the 21-cm topology, rather than the overall level of ionization of the IGM or the delay in the reionization history. The central panel of Figure 6 shows the 21-cm power spectrum at approximately same averaged neutral fraction values ($\bar{x}_{\text{HI}} = 0.84, 0.64$) for different dark matter models (the corresponding redshifts for different dark matter models are tabulated in Table 1). It is obvious from this plot...
that the differences in power spectra between the WDM models and the CDM model become significantly low when compared in this way, and for small $k$ modes (or large length scales), these differences are within the sample variance limits.

To quantify the differences between the EoR 21-cm power spectra from WDM and CDM scenarios, we estimate the quantity $|P_{\text{CDM}} - P_{\text{WDM}}| / P_{\text{CDM}}$. The bottom panel of Figure 6 shows this relative fractional difference in 21-cm power spectrum estimated at same neutral fraction $\bar{x}_{\text{HI}} = 0.84$ and 0.64 between the WDM models and the CDM model. It is clear from this figure that the amplitude of this relative difference is larger for the 2 keV WDM model compared to the 3 keV WDM model. During the early stage of reionization when $\bar{x}_{\text{HI}} = 0.84$, this difference peaks around intermediate length scales and during the intermediate stage of reionization when $\bar{x}_{\text{HI}} = 0.64$ it is peaked around small length scales. We observe that for a large range of $k$-modes, the relative fractional difference varies in the range $0.15 \sim 0.35$ for the comparison between the CDM and the 2 keV WDM, and in the range $0.05 \sim 0.15$ for the comparison between the CDM and the 3 keV WDM model. These differences are probably not large enough to be detectable by the first generation of radio interferometers, which have lower sensitivity. These results are consistent with the previous studies made by Das et al. (2018). Thus, the power spectrum is not an ideal tool to probe the differences between different dark matter models.

4.3 21-cm Bispectrum

The power spectrum is an incomplete statistics when it comes to optimally quantifying the EoR 21-cm signal fluctuations, as this signal is highly non-Gaussian. We use the next higher order statistics, the bispectrum, to quantify this evolving non-Gaussianity in the EoR 21-cm signal. The source of the non-Gaussianity in the signal is the non-random distribution of growing ionized regions in the IGM, which drives the fluctuations in the signal and also leads to the signal correlation between different length scales. We estimate signal bispectrum for all unique $k$-triangles (see Figure 4) for dark matter models to quantify this non-Gaussianity. Figure 7 shows the bispectra at three redshifts $z = (10, 9, 8)$, and for triangles with three $k_1$ modes $k_1 = (0.57, 0.86, 1.30) \text{ Mpc}^{-1}$. We choose not to show the bispectra for $k_1 < 0.57 \text{ Mpc}^{-1}$ because of the high sample variance in these triangle bins (due to our small simulation volume). In an earlier study of the EoR 21-cm bispectrum (in real space) Majumdar et al. (2018) have shown that the bispectrum is mostly negative for triangles involving small $k$ modes. It has a maximum amplitude for the squeezed limit triangles (Majumdar et al. 2018; Hutter et al. 2020). The bispectrum also shows a very interesting feature, it changes its sign when one gradually move from smaller $k$-triangles to triangles with larger $k$ modes. This makes the EoR 21-cm bispectrum an even more interesting statistic for a confirmative detection of the signal (Majumdar et al. 2018; Hutter et al. 2020). However all of these analysis was based on a few specific types of $k$-triangles and for the signal in real space. For a thorough analysis of the EoR 21-cm bispectra for all unique $k$-triangles in redshift space the readers are requested to refer to Majumdar et al. (in prep.).

Based on the plots in Figure 7 and the analysis of Majumdar et al. (2018) and Majumdar et al. (in prep) one can identify few more generic features of the inside-out EoR 21-cm bispectra in the entire unique $k$-triangle space (defined by parameters $n$ and $\cos \theta$), irrespective of the underlying dark matter model. At the very beginning of reionization ($\bar{x}_{\text{HI}} \leq 0.90$) for smaller $k_1$-triangles bispectra for a significant fraction of the $n - \cos \theta$ parameter space is positive and...
in the rest of the parameter space it is negative. For the small $k_1$-triangles as reionization progresses bispectra in most of the $n - \cos \theta$ parameter space becomes negative ($0.85 \geq \bar{x}_{\text{HI}} \geq 0.60$) and stays negative until the $\bar{x}_{\text{HI}} \leq 0.40$. At neutral fractions lower than this the bispectrum starts become positive again in significant portion of the triangle parameter space. Further, for a fixed $\bar{x}_{\text{HI}}$ value as one gradually moves from smaller to larger $k_1$-triangles, a even larger fraction of the $n - \cos \theta$ space starts to have positive bispectrum. The bispectral start to become positive mainly near the squeezed and linear limits ($\cos \theta \approx 1$) of triangles at almost during all stages of the reionization. The amplitude of the bispectra for small $k_1$-triangles reaches a maximum when $\bar{x}_{\text{HI}} \sim 0.5$. The evolution of sign and amplitude of the bispectra can be interpreted in the light of quasi-linear model of brightness temperature fluctuations (Mao et al. 2012). Using this model one can show that there are total eight component bispectra (two auto and six cross) that contributes to the redshift space EoR 21-cm bispectra. Among these eight components the most important ones for the small $k_1$-triangles are the two auto bispectra of the H_I and the matter density field and three cross-bispectra between H_I and matter density fields. These components make the 21-cm bispectra negative in most of the parameter space. The contribution from auto bispectrum of the matter density field is negligible for small $k_1$-triangles. As one moves towards the bispectra for large $k_1$-triangles contribution from the auto bispectrum of the matter density field (which is always positive in sign for all types of triangles) grows and become significantly large at largest $k_1$-triangles and make the 21-cm bispectra positive. For a more detailed discussion on this topic we refer the reader to Majumdar et al. (in prep).

Figure 7 clearly shows that if one compares the bispectra for different dark matter models at the same redshifts, as expected, the differences between them would be quite large. For some $k$-triangles and depending on the stages of the reionization these relative differences can be even larger than the ones observed in case of power spectra. This is due to the fact that as the stages of the reionization are different for different models, the over all level of fluctuations as well the topology will be significantly different, both of which affects the bispectrum amplitude and sign.

### 4.3.1 Difference in 21-cm bispectrum between different models at same mass averaged neutral fraction

For the similar reasons as discussed in case of the power spectra, here also we compare the bispectra for different dark matter models approximately at the same stages of reionization (i.e. $\bar{x}_{\text{HI}} = 0.84$ and 0.64). We estimate the relative differences in the bispectra between the CDM and WDM models by computing the quantity $|B_{\text{CDM}} - B_{\text{WDM}}|/B_{\text{CDM}}$ (Figure 8). It is apparent from Figure 8 that at any stage of reionization, the differences between the 2 keV WDM and CDM models is larger than the differences between the 3 keV WDM and CDM models. For most of the $k$-triangle parameter space ($n - \cos \theta$ space) the relative difference between the 2 keV WDM and CDM models is in between 30–100% or more and for the 3 keV WDM and CDM models the same is in between 10–100% or more. These differences are more prominent for triangles with larger $k_1$ modes compared to the triangles with smaller $k_1$ modes. They are particularly large in the region of the $n - \cos \theta$ space where $n \leq 0.75$ and $0.75 \leq \cos \theta \leq 1.0$.

One important point to note here is that, though we are looking at the 21-cm statistics at almost same stages of reionization in different dark matter models, as the redshifts are different the underlying halo characteristics and distribution will vary from model to model (which can be quantified by their halo mass functions). This differences in the halo mass, their numbers and their spatial distribution will lead to a difference in 21-cm topology across the dark matter models, even when the overall level of ionization remains more or less same in all of these cases. The 21-cm signal power spectrum is expected to be not very sensitive to these differences in topology, however the signal bispectrum will be very sensitive to them as these differences in topology leads to a significant difference in the non-Gaussian characteristics of the signal. One can expect that these significantly larger relative differences in the signal bispectra (compared their relative differences in power spectra), when the underlying dark matter model is different, will be possible to detect with the upcoming highly sensitive SKA. Using sophisticated parameter estimation techniques, while using the signal bispectra as the target statistic, one may be even able to constrain the nature of the dark matter from such future radio interferometric observations of the EoR.

### 5 SUMMARY

In this article we have attempted to quantify the impact of the different kind of warm dark matter models (in comparison with the standard cold dark matter models) on the reionization process and related 21-cm observables such as the power spectrum and bispectrum. We have considered 2 keV and 3 keV thermal WDM models in this context. Using GADGET 2.0 Nbody simulation we observed...
that the non-negligible free streaming of the dark matter particles in the warm dark matter scenarios suppresses the matter density perturbations on small scales (see Figure 1). Further, this suppression was more prominent in the 2 keV WDM scenario compared to the 3 keV WDM model because the lighter the WDM particle, the larger the free streaming scale. We also observed that the effect of this suppressed structure formation gets reflected in the halo mass function of all the dark matter models (Figure 2).

Using a semi-numerical model for reionization, we further observed that due to this suppression of the low mass halos (which are the dominant sources of ionizing photons) the overall reionization of the universe gets delayed in the WDM scenarios compared to the CDM model. This delay is likewise larger in the 2 keV WDM model compared to the 3 keV WDM model, when one keeps the ionizing photon production efficiency of halos same in all dark matter models. The suppression of low mass halo additionally introduces a significant difference in 21-cm brightness temperature topology in case of WDM models compared to the CDM model.

Next, we have quantified the differences in the two observable statistics of the EoR 21-cm signal, power spectrum and bispectrum, for different dark matter models. We found that, if the statistics from different dark models are compared at the same redshifts, the power spectrum differs significantly for both small and large $k$ modes for different matter models. However, when they are compared at the same stage of reionization i.e. at same $\bar{H}_2$ (i.e. by countering the effect of delayed reionization history), the differences in the $P(k)$ become significantly small at all scales between the WDM and CDM models. These become undetectable in case of small $k$ modes as they fall within the sample variance limits.

We have, for the first time, quantified the impact of WDM models on the EoR 21-cm signal using the bispectrum. The bispectrum is expected to be more sensitive to the difference in the dark matter model as it is capable of capturing the non-Gaussian features in the signal to which power spectrum is not sensitive. The source of non-Gaussianity in the EoR 21-cm signal is the evolving $\text{H}^1$ topology during this period, which gets significantly affected by the suppression of the low mass halos in case of the WDM models. We find that the relative differences between the 21-cm bispectra for the WDM and CDM models are larger than their relative differences in the 21-cm power spectrum when compared at the same redshifts. Even when compared at the same stages of the EoR, the relative differences between the EoR 21-cm bispectra for WDM and CDM models varies between 10% – 300% for all unique $k$-triangles. This level of relative differences in 21-cm bispectra for most of the unique $k$-triangle parameter space ensures that one should be able distinguish between the different dark matter models using the future radio interferometric observations of the EoR and this may even help one to constrain the WDM model parameters. Through this analysis we have established that the redshifted 21-cm bispectra is a unique and much more sensitive statistics than the power spectrum for differentiating the impact of different models of dark matter on the reionization process and one may be able to constrain the nature of the dark matter using this statistic from future observations of the CD-EoR through the SKA.

Note that in this work we have not taken into account the impact of spin temperature fluctuations on the EoR 21-cm signal, which may have a significant effect on the 21-cm bispectrum. We have considered only a single model for reionization. However, the 21-cm topology and the resulting non-Gaussianity in the signal may change significantly if we change our reionization model. All of these effects will affect the 21-cm bispectrum. However, even if we take into account all of these effects into our formalism for a more accurate model of the EoR 21-cm signal, we expect that the differences in different dark matter models will still be prominently visible in the 21-cm bispectra.

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APPENDIX A: DIFFERENCES IN THE OBSERVABLE STATISTICS OF THE 21-CM SIGNAL WITH DIFFERENT IONIZING EFFICIENCY FOR DIFFERENT MODELS

In this appendix, we repeat our analysis by varying the ionizing efficiency parameter $\gamma_{\text{ion}}$ in different dark matter models to ensure that we obtain the same $x_{\text{HI}}$ for all of these models in the same redshifts. We choose the $\gamma_{\text{ion}}$ values such that (Table A1) in all models universe becomes 50% ionized by redshift 8.

A1 21-cm topology

In Figure A1, we have shown the 21-cm brightness temperature maps at $z = 8$ with mass averaged neutral fraction $\bar{x}_{\text{HI}} \approx 0.5$ for all the models. We observe that the 21-cm topology has significant similarity at large scales, however, it has quite a few differences at small length scales for different models of dark matter. The size of ionized bubbles is relatively larger in WDM models compared to the CDM model. This is an obvious signature of the suppression in the number of low mass halos in WDM models compared to their CDM counterpart. The lack of the low mass halos have been compensated by increasing the ionizing photon production efficiency (see Table A1) in all halos in these models. This implies that the high mass halos in WDM models will produce significantly more photons compared to their counterparts in CDM model and will thus produce larger ionized bubbles (compare the three panels in Figure A1). These features have also been reported by Das et al. (2018).

| Table A1. This tabulates the $\gamma_{\text{ion}}$ values required in different dark matter models to ensure that $x_{\text{HI}} = 0.5$ at $z = 8$ |
|----------------|----------------|----------------|
| Model          | 3 keV WDM      | 2 keV WDM      |
| CDM            | 23.21          | 33.70          |
| 3 keV WDM      | 47.50          | 47.50          |

![Figure A1. 21-cm brightness temperature maps at $z = 8$ with mean neutral fraction $\bar{x}_{\text{HI}}$ = 0.47 for CDM (left), 3 keV WDM (middle) and 2 keV WDM (right).](image1)

![Figure A2. 21-cm power spectrum at $z = 8$ with mean neutral fraction $\bar{x}_{\text{HI}}$ = 0.47 in CDM (red), 3 keV WDM (blue) and 2 keV WDM model (green).](image2)
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Figure A3. Relative fractional difference in 21-cm bispectra between CDM and 2 keV WDM model (Top panel), and between CDM and 3 keV WDM model (Bottom Panel) at \( k_1 = 0.57, 0.86 \) and \( 1.30 \) Mpc\(^{-1} \) (left to right) at mass averaged neutral fraction \( \bar{x}_{\text{HI}} = 0.47 \).

A2 Observable statistics of the 21-cm signal

A2.1 21-cm power spectrum

Figure A2 shows the 21-cm power spectrum for different dark matter models at \( \bar{x}_{\text{HI}} \approx 0.5 \). We observe that the 21-cm power spectrum in WDM models is greater than that in the CDM model. This is because in WDM models, the ionized bubbles are larger in size (due to the increased \( N_{\text{ion}} \) value). One can also notice that the difference in 21-cm power spectra between different models remains significantly low even if we change our reionization model, and at large scales these differences are within the sample variance limit.

A2.2 21-cm bispectrum

In Figure A3, we have shown the relative fractional difference in 21-cm bispectra between the CDM and WDM models at \( k_1 = 0.57, 0.86 \) and \( 1.30 \) Mpc\(^{-1} \). One obvious observation that one can make is that these differences in bispectra are larger when estimated between CDM and 2 keV WDM model.

Further, these differences are larger than those observed in Figure 8. This is because by changing the \( N_{\text{ion}} \), we are changing our reionization model. Note that even at large scales \( k_1 = 0.57 \) Mpc\(^{-1} \), the differences are large for most of the unique \( k \) triangles. Additionally, at relevant small scales (or large \( k_1 \) values), the differences are also quite large due to the fact that the strength of 21-cm signal gets increased in WDM models at small scales.

We conclude that even when one changes the reionization source model to arrive at same state of IGM ionization at the same redshift for different dark matter models, the bispectrum remains equally or more sensitive to the characteristics of the dark matter model. However, power spectrum remains equally insensitive to the dark matter model characteristics in this case as well.

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