K2 Ultracool Dwarfs Survey. II. The White Light Flare Rate of Young Brown Dwarfs

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Received 2017 March 25; revised 2017 June 23; accepted 2017 July 3; published 2017 August 9

Abstract

We use Kepler K2 Campaign 4 short-cadence (one-minute) photometry to measure white light flares in the young, moving group brown dwarfs 2MASS J03350208+2342356 (2M0335+23) and 2MASS J03552337+1133437 (2M0335+11), and report on long-cadence (thirty-minute) photometry of a superflare in the Pleiades M8 brown dwarf CFHT-PL-17. The rotation period (5.24 hr) and projected rotational velocity (45 km s⁻¹) confirm 2M0335+23 is inflated (R ≳ 0.20 R☉) as predicted for a 0.06 M☉, 24 Myr old brown dwarf βPic moving group member. We detect 22 white light flares on 2M0335+23. The flare frequency distribution follows a power-law distribution with slope −α = −1.8 ± 0.2 over the range 10⁻³⁵ to 10⁻¹⁸ erg. This slope is similar to that observed in the Sun and warmer flare stars, and is consistent with lower-energy flares in previous work on M6–M8 very-low-mass stars; taking the two data sets together, the flare frequency distribution for ultracool dwarfs is a power law over 4.3 orders of magnitude. The superflare (2.6 × 10⁻¹⁸ erg) on CFHT-PL-17 shows higher-energy flares are possible. We detect no flares down to a limit of 2 × 10⁻¹⁰ erg in the nearby L5γ AB Dor moving group brown dwarf 2M0355+11, consistent with the view that fast magnetic reconnection is suppressed in cool atmospheres. We discuss two multi-peaked flares observed in 2M0335+23, and argue that these complex flares can be understood as sympathetic flares, in which fast-mode magnetohydrodynamic waves similar to extreme-ultraviolet waves in the Sun trigger magnetic reconnection in different active regions.

Key words: brown dwarfs – stars: activity – stars: flare – stars: individual (2MASS J03350208+2342356, 2MASS J03552337+1133437) – starspots

1. Introduction

The paradigm for the evolution of magnetic activity in low-mass main sequence stars is that magnetic braking causes the initially rapid rotation from pre-main sequence contraction to gradually decline, and this in turn causes the magnetic fields generated by the dynamo to weaken (Donati & Landstreet 2009). As a result, both the rotation rate and magnetic activity such as flaring decrease with age (Gershberg 2005; Telleschi et al. 2005). For fully convective 0.3 M☉ stars, half the angular momentum is shed between 3 Myr and the Pleiades age (Stauffer et al. 2016). The rotation and magnetic activity evolution of brown dwarfs is quite different. Measurements of v sin i for field brown dwarfs (Zapatero Osorio et al. 2006; Reiners & Basri 2008) imply a mean rotation period of 4.1 hr (Radigan et al. 2014), and a large sample of mid-infrared photometric periods confirm this view (Metchev et al. 2015). All of these are rapid rotators compared to field stars. Christensen et al. (2009) show that turbulent dynamos can generate magnetic fields in stars, brown dwarfs, and planets, and that provided the object is rapidly rotating, the strength of the magnetic fields is determined by the energy flux. Reiners & Christensen (2010) show this theory implies that massive brown dwarfs have fields of a few kilogauss in their first few hundred million years, weakening to fields of 100–1000 G by an age of 10ⁱ⁰ yr. Simulations of the turbulent dynamo in fully convective stars show that both large-scale dipole and small-scale magnetic fields are generated (Yadav et al. 2015). Overall, the expectation is that all brown dwarfs have significant magnetic fields, and indeed radio observations support the existence of magnetic fields even in cool T-type brown dwarfs (Route & Wolszczan 2012; Williams & Berger 2015).

Despite the presence of strong magnetic fields, the fraction of a star’s or brown dwarf’s energy converted into chromospheric activity weakens for “ultracool dwarfs” with temperatures below the M6 spectral type (Gizis et al. 2000; Schmidt et al. 2015). Mohanty et al. (2002) have shown this can be understood as a consequence of the increasingly neutral atmospheres: as the ionization fraction drops and the resistance increases, the magnetic fields become decoupled from the matter. These were equilibrium calculations and, as Mohanty et al. (2002) noted, the existence of flares implies transient, time-dependent processes are important. A transition from fast magnetic reconnection at high temperatures to a high-resistivity regime where only slow magnetic reconnection is allowed may explain the decline in chromospheric and coronal activity but continued radio emission (Mullan 2010). This scenario sees the fast reconnection events resulting in a range of energy release events, from many nanoflares that heat the chromosphere and corona to rarer but more powerful white light flares that can be individually observed. Additional parameters seem to be important in magnetic activity: magnetic topology may explain the difference between radio-quiet, X-ray-bright dwarfs and radio-loud, X-ray-faint dwarfs (Cook et al. 2014; Williams et al. 2014).

Even setting aside the numerous radio-only bursts, it is well established that X-ray and optical flares do occur in stellar late-M and early-L dwarfs—some notable examples include the very first optical spectrum of V810, the first known M8 dwarf (Herbig 1956), the discovery of a nearby M9 dwarf due to a huge X-ray flare with Lx/Lbol = 0.1 (Hambaryan et al. 2004), and an L0 dwarf with a ΔV < −11 white light flare (Schmidt et al. 2016). The serendipitous optical spectra of the M7–M9 dwarf flares reported by Bessell (1991), Martín (1999), Liebert et al. (1999),
Reid et al. (1999), Gizis et al. (2000), and Martin & Ardila (2001) all showed strong atomic emission lines and many included veiling or a blue continuum. A difficulty, however, with flare studies is that detectable flares are so rare that it is difficult to assess their frequency as a function of energy. Hilton (2011) monitored four field M6–M8 stars in the U-band and found 39 flares over 59 hr. These flares followed a power-law frequency distribution, as seen in hotter flare stars, but with a rate comparable to “inactive” but more luminous M0–M2.5 dwarfs. Similarly, Kepler optical monitoring of a L1 dwarf star also found a power-law flare frequency distribution (Gizis et al. 2013). Young M-type brown dwarfs with similar Lbol also exhibit flares, such as the ~500 Myr M9 lithium brown dwarf LP 944-20 (Rutledge et al. 2000). X-ray flares, as well as quiescent emission, have also been reported from very young (<5 Myr) M6–M9 brown dwarfs in Orion (Preibisch et al. 2005) and Taurus (Grosso et al. 2007).

By monitoring over 100,000 stars over four years, the Kepler mission (Koch et al. 2010) is known to have detected over 800,000 flares in 4041 stars (Davenport 2016). These include superflares in A and F stars with thin convective zones (Balona 2012, 2015) and solar-like G dwarfs (Maehara et al. 2012) as well as fully convective M dwarfs (Martin et al. 2013; Hawley et al. 2014) and even an L1 dwarf (Gizis et al. 2013). These flares are detected by white light emission enhancing the normal stellar photospheric emission. The presence of lithium identified this object unambiguously as a brown dwarf (Rebolo et al. 1992). Shkolnik et al. (2012) measured its trigonometric parallax distance to be 42.4 ± 2.3 pc and showed that its distance and space velocity identified it as a member of the β Pic moving group (BPMG). The latest parallax from Liu et al. (2016) places it at 46 ± 4 pc; for consistency with the literature we adopt the nominally more precise distance of 42.4 pc for our analysis. The age of this group is 24 ± 3 Myr (Mamajek & Bell 2014; Bell et al. 2015). Gagné et al. (2015a) have analyzed 2M0335+23 in detail to find that it is 60.9±4.4 Jupiter masses (i.e., 0.058 ± 0.004 M⊙) with a radius of 2.40 ± 0.04 Jupiter radius according to models (Gagné et al. 2015a). Adopting 

$$B_G = 2.0 \text{ (Filippazzo et al., 2015), the luminosity is } 10^{-2.55} L_\odot$$

and $T_{\text{eff}} = 2700 \text{ K}$. Sarro et al. (2014) measured it to have apparent (AB) magnitude $i = 15.601 \text{ (source DANCe 5121623).}$ Infrared spectroscopy confirms that it has lower surface gravity than ordinary field dwarfs, with a classification of M7 VL-G (Allers & Liu 2013) and M7.5β (Gagné et al. 2015a). In the optical, low surface gravity leads to enhanced VO features (Kippenhahn et al. 2008); this would bias Gizis et al.’s (2000) classification to a later type. We re-classify the spectrum as M7/β in the optical. In particular, the optical spectrum of 2M0335+23 is definitely “earlier” (warmer) than the young M9 brown dwarf 2MASS J06085283-2753583 (Cruz et al. 2003) which may be a BPMG member (Rice et al. 2010) or more likely a 40 Myr old Columba member (Liu et al. 2016). The observed Hα emission line strength of EW $\approx 5$ Å implies log $H\alpha/L_{\text{bol}} \approx -5.5$ (Schmidt et al. 2014b). Despite 2M0335+23’s rapid rotation and youth, this places it in the bottom half of the M7 activity range (Schmidt et al. 2014a).

Finally, we use the mass, luminosity, and radius to predict the theoretical mean surface magnetic fields of our targets using Equation (1) of Reiners & Christensen (2010). 2MASS J03552337+1133437 (hereafter 2M0355+11) was observed by K2 as source EPIC 210327027. Discovered by Reid et al. (2006) and classified as low surface gravity (L5γ) with lithium by Cruz et al. (2009), this brown dwarf is now recognized as a dusty, low surface gravity member of the AB Doradus moving group (ABDMG) which shares many spectral characteristics with directly imaged exoplanets (Faherty et al. 2013; Liu et al. 2013). Bell et al. (2015) derived an ABDMG age of 149±19 Myr; note that this age is tied to the Pleiades age of 130 ± 20 Myr from lithium depletion (Barrado Navascués et al. 2004) which has been updated to 112 ± 5 Myr (Dahn 2015). Liu et al. (2016) measured a trigonometric parallax of 109.5 ± 1.4 mas, and we use a distance of 9.1 pc for the rest of this paper. For discussion purposes, we adopt the values derived by Filippazzo et al. (2015): log $L/L_{\odot} = -4.10 \pm 0.03$, radius $R = 1.32 \pm 0.09 R_\odot$, surface gravity log $g = 4.45 \pm 0.21$, $T_{\text{eff}} = 1478 \pm 57 \text{ K}$, and mass $M = 19.98 \pm 7.76 M_\oplus$ (i.e., $\approx 0.02 M_\odot$). Blake et al. (2010) measured $\sin i = 12.31 \pm 0.15 \text{ km s}^{-1}$, noting that it is an unusually slow rotator for an L dwarf. This, however, still implies a minimum rotation period of 13 hr, a rapid rotator compared to M dwarf stars. No Hα emission has been detected (EW $\approx 24.29 \text{ Å}$, Schmidt et al. 2007) though the upper limit is above the emission level of most L dwarfs.

2. Targets and Spectroscopy

2.1. Target Characteristics

In Table 1, we list the key properties of our targets. 5 2MASS J03350208+2342356 (hereafter 2M0335+23) was observed by K2 as source EPIC 211046195. This field ultracool dwarf was discovered by Gizis et al. (2000), who classified it as M8.5 in the optical and noted Hα emission. It is apparently single in the Hubble Space Telescope (HST) imaging (Gizis et al. 2003). Reid et al. (2002) detected significant rotational broadening ($v \sin i \approx 30 \text{ km s}^{-1}$), lithium in absorption, and again detected Hα emission. The presence of lithium identified this object unambiguously as a brown dwarf (Rebolo et al. 1992). Shkolnik et al. (2012) measured its trigonometric parallax distance to be 42.4 ± 2.3 pc and showed that its distance and space velocity identified it as a member of the β Pic moving group (BPMG). The latest parallax from Liu et al. (2016) places it at 46 ± 4 pc; for consistency with the literature we adopt the nominally more precise distance of 42.4 pc for our analysis. The age of this group is 24 ± 3 Myr (Mamajek & Bell 2014; Bell et al. 2015). Gagné et al. (2015a) have analyzed 2M0335+23 in detail to find that it is 60.9±4.4 Jupiter masses (i.e., 0.058 ± 0.004 M⊙) with a radius of 2.40 ± 0.04 Jupiter radius according to models (Gagné et al. 2015a). Adopting 

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5 EPIC 211046195 and EPIC 210327027 were observed for K2 Guest Observer Program 4036 (PI Gizis); EPIC 211110493 was observed for GO Programs 4024 (PI Lodieu), 4026 (PI Scholle), and 4081 (PI Demory).
Table 1

| Object          | EPIC   | \(K_p\) | Type | Distance | Age   | Mass   | \(\log L/L_{\odot}\) | \(T_{\text{eff}}\) | \(B\) |
|-----------------|--------|---------|------|----------|-------|--------|----------------------|-------------------|------|
| 2M0335+23       | 211046195 | 16.7    | M7/β | 42.4 pc  | 24 Myr | 0.06 \(M_{\odot}\) | −2.55               | 2700 K           | 2.2 kG |
| 2M0355+11       | 210327027 | 20.4    | L5γ  | 9.1 pc   | 150 Myr| 0.02 \(M_{\odot}\) | −4.10               | 1480 K           | 1.1 kG |
| CFHT-PL-17      | 211110493 | 20.8    | M6/β | 136 pc   | 112 Myr| 0.06 \(M_{\odot}\) | −3.07               | 2500 K           | 2.5 kG |

Note. Parameters given are rounded off. The mean surface magnetic field \(B\) is theoretical. See the text for references and uncertainties.

CFHT-PL-17, a brown dwarf member of the Pleiades discovered by Bouvier et al. (1998), was observed by \(K_2\) as source EPIC 211110493. Martín et al. (2000) classified it as optical spectral type M7.9 (which we will hereafter round off to M8.) and found Hα emission (EW \(\approx 7\) Å). Bouy et al. (2015) confirm it has a 100% chance of being a cluster member and measure \(i = 19.745\) (AB). We adopt the VLBI Pleiades distance of 136.2 ± 1.2 pc (Melis et al. 2014); Bouy et al. (2015) using the same distance, find a luminosity of 0.0008456 \(L_{\odot}\) \((T_{\text{eff}} = 2500\) K) which implies the mass is 0.06 \(M_{\odot}\). Thus, CFHT-PL-17 is very similar in mass to 2M0335+23, but older and one spectral type later (~200 K cooler), and it is a similar age to 2M0355+11, but more massive and warmer.6

2.2. New Spectroscopy

We observed 2M0335+23 on UT date 2016 February 3 with the Keck NIRSPEC spectrograph (McLean et al. 2000) to obtain spectra with \(\lambda/\Delta \lambda = 20,000\) in the 2.3 \(\mu m\) region dominated by CO bands. Conditions were clear with 1″ seeing. We obtained two exposures of 750 s each, following observation of the A0V star HD 19600 for telluric calibration. We achieved a typical signal-to-noise of 23 on UT date 2016 February 3 with \(\lambda = 2.15\mu m\). A set of radial velocities were measured for 2M0335+23 with a velocity error of 1.0 km s\(^{-1}\). The radial velocity increases 2M0335+23’s probability of BPMG membership to 96.5% using the Shkolnik et al. (2012) astrometry in the BANYAN II model (Gagné et al. 2014, 2015b).

3. \(K_2\) Photometry

Kepler records the pixels for every target as averages over “long” (30 min, Jenkins et al. 2010) cadences; for 2M0335+23 and 2M0355+11, it also recorded “short” (1 min, Gilliland et al. 2010) cadence data. We report Kepler mission times, which are equal to BJD—2454833.0.

The brightnesses of \(K_2\) and \(K_2\) targets are described on the \(K_p\) magnitude system (Brown et al. 2011) tied to ground-based photometry; this system was not designed for ultracool dwarfs and the EPIC catalog (Huber et al. 2016) magnitudes for our targets are not useful. Lund et al. (2015) defined \(\bar{K}_p = 25.3 - 2.5 \log (flux)\), where \(\bar{K}_p \approx K_p\) for most (e.g., AFGK-type) stars and “flux” is the count rate measured through a 3 pixel radius aperture. We find that the apparent \(\bar{K}_p\) magnitudes of 2M0335+23, 2M0355+11, and CFHT-PL-17 are 16.7, 20.4, and 20.8. Using \(\bar{K}_p\) we can discuss both extremely red sources and time-dependent (blue) flares in terms of the well established \(K_p\) system.

2M0335+23 is bright enough that photospheric variability is detectable. We use the \(K_2\) mission pipeline photometry corrected for the effects of pointing drift and other systematic errors. For 2M0335+23, the Lomb–Scargle periodogram shows a strong signal at \(P = 0.2185\) days (5.244 hr), which we identify as the rotation period of the brown dwarf. The phased data are shown in Figure 1 normalized to the median. We have verified that other \(K_2\) pipelines (Vanderburg & Johnson 2014; Aigrain et al. 2016; Armstrong et al. 2016) give consistent results for this source. We do not detect periodic photometric variations in 2M0355+11 or CFHT-PL-17. We note that in the case of the \(K_2\) mission corrected photometry for 2M0355+11, there is a periodic signal of 1.11 days, but we believe this is a spurious signal, and it is not present in the other reduction pipelines.

We measured short-cadence photometry using the \(K_2\) Release 10 pixel files. (There is not yet any \(K_2\) mission official light curve product for short-cadence data.) We used circular aperture photometry (photutils) with radius of 2 pixels centered on the target, but we verified that our results are qualitatively unchanged with circular apertures of radius 3 or rectangular fixed apertures. The sources, especially 2M0355+11, are faint enough that centroiding introduces photometric noise; we adopt a best position based on the median of all centroid measurements, and then adjust it for each observation using the spacecraft motion estimate calculated by the mission (recorded as POS_CORR1 and POSS_CORR2 in the FITS file headers). The photometry shows the usual systematic drifts, but these have little effect on measurements of flares which have timescales of a few minutes.

6 We also identify a flare in the candidate Pleiades brown dwarf BPL 76 (Pinfield et al. 2000), observed as EPIC 211000317. Bouy et al. (2015), however, have measured its proper motion and assign it a membership probability of zero.
We lack short-cadence photometry for CFHT-PL-17, but motivated by the strong flare at mission day 2261.94 which we noticed in the mission pipeline photometry, we measured our own 2 pixel radius long-cadence photometry in the same way to analyze its flare. We identified 22 flares in 2M0335+23 by visually examining the lightcurves; they are shown in Figure 2 and listed in Table 2. We reject all events that brighten in only a single observation or are not centered on the target's position. No flares are detected in 2M0355+11; we note however that a passing asteroid creates a spurious brightening in aperture photometry at mission time 2271.13.

For each 2M0335+23 flare, we fit the M dwarf flare light curve described by Davenport et al. (2014), hereafter D14, who found that most flares on the M4 dwarf GJ 1243 could be described by a fast rise (a fourth-order polynomial) and a slower double exponential decay:

\[ \Delta F = A (\alpha_f e^{-\gamma_f \Delta t / \tau_f^2} + \alpha_s e^{-\gamma_s \Delta t / \tau_s^2}) \]

All flare light curves are then described by nine universal parameters: \( \alpha_f = 0.6890 \pm 0.0008 \), \( \alpha_s = 0.3030 \pm 0.0009 \), \( \gamma_f = 1.6000 \pm 0.0003 \), \( \gamma_s = 0.2783 \pm 0.0007 \) plus the five polynomial parameters given in D14. Each flare also has three unique parameters: the peak amplitude of the flare, the full-width time at half-maximum (\( \tau_f / 2 \)), and the time of the flare peak. We fit four free parameters to each flare using emcee (Foreman-Mackey et al. 2013): the non-flaring photosphere, the peak amplitude of the flare, the full-width time at half-maximum (\( \tau_f / 2 \)), and the time of the flare peak. The fits are shown in red in Figure 2. Two of the brighter flares (on mission days 2240 and 2287) are complex flares with two peaks in their light curves: We have fit them as the superposition of two flares. The equivalent duration listed in Table 2 is a measure of the flare energy compared to the quiescent luminosity; it is obtained by integrating the observed flare count rate and dividing by the photosphere count rate. This is a distance-independent measure of the flare, but it is dependent on the filter and the photospheric properties of the stars. Our durations will be much longer than otherwise identical flares observed on a G dwarf due to the lower photospheric flux. Our detection of weak flares is limited by noise, and it is clear that we cannot reliably detect flares below equivalent durations of 20 s. The flares on mission days 2238, 2249, and 2251 in Figure 2 are examples of marginal detections that may be some form of correlated noise rather than real flares. The flare on mission day 2299 is also questionable because most of the flux occurs in a single time period; its exclusion would have a negligible effect on the remaining analysis.

The strongest 2M0335+23 flare (mission time 2253.65107) has noticeable deviations from the D14 template: The best-fitting model (red) under-predicts the peak and over-predicts the gradual phase, with a \( \tau_f / 2 \) that is too short. We therefore use a new model template in which we keep the polynomial rise parameters fixed but allow the decay parameters to be fitted. This adds three free parameters, since we require \( \alpha_f + \alpha_s = 1 \). The results are: \( \alpha_f = 0.9233 \pm 0.0055 \) \( \alpha_s = 0.0767 \), \( \gamma_f = 1.3722 \pm 0.054 \), and \( \gamma_s = 0.1163 \pm 0.011 \). Gershberg (2014) argues that, during the impulsive decay phase, cooling is by blackbody emission, which suggests the relative contribution of this component of radiative cooling was different in this flare.

To calibrate the equivalent duration in terms of energy, we follow the procedures described in Gizis et al. (2013). Because flares are much hotter than the brown dwarf targets, white light flares have a higher average energy per detected K2 photon than the photosphere. The photosphere is modeled with an active M7 dwarf template (Bochanski et al. 2007) scaled to the measured \( i \) photometry and known trigonometric parallax distance. The flare is modeled as an 10,000 K blackbody, which gives good agreement with the flare measurements in Hawley & Pettersen (1991). Figure 3 shows the optical and near-infrared spectral energy distribution of 2M0335+23 and flare with the same count rate through the Kepler filter. We find that a flare with equivalent duration of 1 s has a total bolometric UV/Vis/IR energy of \( 2.0 \times 10^{30} \) erg. We emphasize that we have extrapolated to wavelengths not detected by K2 and that our analysis includes atomic emission features between 430 nm and 900 nm in the observed “white light” photometry. Finally, we also report the peak (short-cadence) absolute \( K_p \) magnitude of the flare. For these, we have applied an aperture correction of 1.08 to correct the \( r = 2 \) pixel aperture to the \( r = 3 \) pixel aperture. We note that the total equivalent duration of detected flares is 0.030 days, so that just 0.04% of the 2M0335+23’s optical light over the course of the campaign is due to white light flares.

We detected no flares in 2M0355+11. We verified that we could have detected flares by adding our observed 2M0335+24 flare data back into the 2M0355+11 at random times, and recovered them all. Because 2M0355+11 is 4.7 times closer than 2M0335+24, a flare with 22 times less energy would produce the same count rate. We conclude that we could have detected flares with \( E > 2.0 \times 10^{30} \) erg, and place a 95% confidence upper limit of three such flares over 70.7 days. (The effect of 2M0355+11 photosphere’s much fainter apparent magnitude would be simply to increase the equivalent duration or relative amplitude of the flare.) If the timescale for these flares, however, was less than one minute than we could not distinguish them from cosmic rays or other noise sources. However, because the late-M dwarf flares (Hilton 2011, Table 4.1) with energies at or above our limit have timescales of several minutes, we conclude that this effect is not a concern.

We measure the flare on CFHT-PL-17 using 3 pixel radius aperture photometry (Figure 4). The flare is first detectable at mission time 2261.9407 where it has brightened to 9.0 times the original photosphere. In the 2261.9612 exposure, it has reached 77 times the photosphere to achieve \( K_p = 16.0 \). The flare then declines, with the last detectable excess of 24% at 2262.1246, for a total observed duration of 5 h. The equivalent duration is 170,000 s (2.0 days). Using the same calibration procedure with an active M8 template (Bochanski et al. 2007), we calculate the flare energy is 2.6 \( \times 10^{34} \) erg. Given the sharply peaked light curve, we conclude that \( \tau_f / 2 < 30 \) min.

We can fit the D14 template by computing it in one minute timesteps but comparing to the long-cadence data, as in our analysis of an L dwarf superflare in Paper I of this series (Gizis et al. 2017). We find that the peak is 380 times the photosphere (\( K_p \approx 14.3 \)), with \( \tau_f / 2 \) of 3.9 minutes. This should be viewed with caution because we do not know if the D14 template applies to this flare, or if the flare was complex and multi-peaked. On the other hand, Kepler short-cadence photometry of comparable energy flares in F stars shown by Balona (2012) are sharply peaked.

4. Discussion

4.1. The Radius of a 24 Myr Brown Dwarf

Young brown dwarfs should have inflated radii compared to field stars of the same spectral type. Our measured rotation...
period and measured $v \sin i$ together imply that $R \sin i = 0.196 \pm 0.015 R_\odot$ for 2M0335+23, whose age of $24 \pm 3$ Myr is independently known. This is much larger than the radii of field M7 dwarfs, which have have $R = 0.12 R_\odot$ (Dieterich et al. 2014). This result can be seen as either an independent confirmation of the the evolutionary model prediction that young brown dwarfs are larger or, if the models are trusted, as independent support for BPMG group membership of 2M0335+23. Using the previously estimated radius of Gagné et al. (2015a), we find that the inclination is $i = 54.4 \pm 6.6$.

4.2. Flare Frequency Distribution

Studies of flare stars have found that the cumulative flare frequency distribution (FFD) follows a power-law trend (Gershberg 1972; Lacy et al. 1976). We compute the cumulative frequency ($\nu$) of 2M0335+23 flares as the number ($N$) observed with a given energy or greater divided by the total time of observation (70.7 days) and plot the results in in Figure 5. The statistical properties of power-law (“Pareto”) distributions are reviewed by Arnold (2015). We consider both the graphical technique of fitting a line to Figure 5 and
dependence is

\[ dN \propto E^{-\alpha}dE. \]  

(3)

Here \( dN \) is the number of events between energy \( E \) and \( E+dE \). As often discussed for flares, if \( \alpha > 2 \) the total energy in small events (nanoflares) would diverge. Because \( \beta = -\alpha + 1 \), giving \( \alpha = 1.7 \) for 2M0335+23. We plot limits on the FFD for the L5\( \gamma \) brown dwarf 2M0355+11. We also show the Kepler L1 dwarf W1906+40 (Gizis et al. 2013) FBD but over the energy range \( 10^{31} \) erg to \( 2 \times 10^{32} \) erg. For this star, \( a = -1.35 \pm 0.06 \) and \( \beta = -0.59 \pm 0.09 \), but we caution that the slope depends sensitively on the energy range chosen.

An alternative approach is to use the maximum likelihood estimator for \( \alpha \) (Arnold 2015):

\[ (\alpha - 1) = n \left[ \sum_{i=1}^{n} \ln \frac{E_i}{E_{\text{min}}} \right]^{-1}, \]  

(4)

where for 2M0335+23 case \( n = 19 \) and \( E_{\text{min}} = 4.66 \times 10^{31} \) erg. The uncertainty in this estimator can also be calculated (we used the software from Alstott et al. 2014). Because our sample is relatively small the uncertainty is large (\( \pm 0.2 \)) and, importantly, the estimator is biased. Arnold (2015) shows it can be made unbiased by multiplying it by a factor of \( \frac{n}{n-2} \), giving \( \alpha = 1.79 \pm 0.21 \). We conclude that the maximum likelihood estimate of \( \alpha \) is consistent with the linear fit value. We adopt the (larger) uncertainty of \( \pm 0.2 \) from the maximum likelihood estimator. For W1906+40, the maximum likelihood estimator is \( \alpha = 1.6 \pm 0.2 \).

The 2M0355+11 limit is shown in red in Figure 5. If one assumes 2M0355+11 would follow the same power-law slope as 2M0335+23 or W1906+40, then the red dashed line

\begin{table}[h]
\centering
\caption{Flares in 2M0335+23}
\begin{tabular}{|c|c|c|c|c|c|}
\hline
Time & Peak Ratio & Equation Duration & Energy (10^{31} erg) & Secondary Time & Comments \\
(d) & & (s) & & (days) & \\
\hline
2253.65107 & 1.83 & 518 & 103.5 & ... & ... \\
2240.04075 & 0.68 & 494 & 98.9 & 2240.0511 & Complex \\
2281.57290 & 1.47 & 339 & 67.8 & ... & ... \\
2284.68258 & 1.69 & 267 & 53.4 & ... & ... \\
2287.91009 & 0.22 & 203 & 40.5 & 2287.9161 & Complex \\
2268.87127 & 0.20 & 145 & 29.0 & ... & ... \\
2295.39965 & 0.75 & 110 & 22.0 & ... & ... \\
2299.37770 & 0.66 & 56 & 11.2 & ... & Questionable \\
2291.45770 & 0.38 & 53 & 10.7 & ... & ... \\
2248.59421 & 0.24 & 48 & 9.6 & ... & ... \\
2261.51045 & 0.23 & 47 & 9.4 & ... & ... \\
2269.02792 & 0.15 & 35 & 7.0 & ... & ... \\
2249.17243 & 0.11 & 35 & 6.9 & ... & ... \\
2276.02709 & 0.17 & 32 & 6.4 & ... & ... \\
2229.08574 & 0.07 & 28 & 5.5 & ... & ... \\
2293.30131 & 0.13 & 26 & 5.2 & ... & ... \\
2295.02755 & 0.15 & 25 & 5.0 & 26 & 5.0 \\
2258.54786 & 0.04 & 24 & 4.8 & ... & Complex? \\
2284.92844 & 0.09 & 23 & 4.7 & ... & ... \\
2238.85706 & 0.11 & 18 & 3.5 & ... & ... \\
2251.42265 & 0.05 & 13 & 2.6 & ... & Questionable \\
2249.41148 & 0.05 & 10 & 1.9 & ... & Questionable \\
\hline
\end{tabular}
\end{table}

Figure 3. Optical and near-infrared spectral energy distribution of 2M0335+23 in red with a hypothetical 10,000 K blackbody that produces the same \textit{Kepler} count rate. The infrared spectrum is from Allers & Liu (2015) and the optical is an M7 standard (Bochanski et al. 2007) scaled to the photometry. Using the distance of 42.4 pc, the bolometric luminosity of 2M0355+23 is \( 1.1 \times 10^{33} \) erg s\(^{-1}\), mostly emitted longward of the broad \textit{Kepler} optical filter, and the flare is \( 2.0 \times 10^{30} \) erg s\(^{-1}\), much emitted shortward.

maximum likelihood estimation: Arnold (2015) notes that the two techniques are consistent and that the traditional graphical technique is “only slightly inferior” to the maximum likelihood estimates. Considering flares in the energy range \( 4 \times 10^{31} \) erg to \( 1.1 \times 10^{33} \) erg, using frequency units of day\(^{-1}\), and weighting each point by \( \sqrt{N} \), we fit a linear relationship

\[ \log \nu = a + \beta \log(E/10^{32} \text{erg}). \]  

(2)

We find \( \beta = -0.66 \pm 0.04 \) and \( a = -0.83 \pm 0.01 \) for 2M0335+23. An alternative expression of this power-law
erg, where the frequency in h \(=\) over the range 0–20.49 3.

\(\text{Figure 4.} \) K2 images of the Pleiades brown dwarf CFHT-PL-17 at the flare peak (top left) and 2.5 hr before (bottom left) and the light curve of the flare (right). Each photometric data point is the average brightness over a 30 min window. The photometry peaks at 77 times the non-flaring photosphere at mission time 2261.9612. If sampled on short cadence, the peak would have been considerably brighter.

\(\text{Figure 5.} \) Observed flare frequency distribution (FFD) and fit for the brown dwarf 2M0335+23 (black points and dashed line) compared to the L1 dwarf W1906+40 (blue) and upper limit for 2M0355+11 (red). The Hilton (2011) fit to the FFD for field M6–M8 dwarfs, transformed from \(E_U\) to total energy as described in the text is also shown. The Hilton (2011) slope and normalization agree remarkably well with 2M0335+23’s FFD measured at higher energies.

upper limit shown in Figure 5 applies. In any case, 2M0355+11’s incidence of flares of \(2 \times 10^{32}\) erg or greater is less than 13% that of 2M0335+23 and less than 40% that of the much older star W1906+40.

Hilton (2011) found that for four M6–M8 dwarfs, \(a = 20.49 \pm 3.3\) and \(\beta = -0.73 \pm 0.1\) over the range \(10^{27.94} \leq E_U \leq 10^{30.60}\) erg, where the frequency in h\(^{-1}\) is the energy in the U-band, and the reported intercept \(a\) is at zero energy, not \(10^{32}\) erg. In order to compare this FFD, we can make a crude energy correction by noting that Hawley & Pettersen (1991) found that the total energy of an AD Leo flare was \(806/145 = 5.55\) times greater than the U-band energy (their Table 6). (The 10,000 K blackbody agrees well with this flare, see Gizis et al. 2013). Applying this correction, the Hilton (2011) relation agrees remarkably well not only in slope but also normalization (Figure 5). The agreement in normalization seems rather fortuitous given the uncertain energy corrections applied, the combination of multiple stars, and the fact that as a young brown dwarf, 2M0335+23 is both larger and more luminous than a field M7 dwarf.

We conclude that the flares for ultracool dwarfs follow a power law over the range \(5 \times 10^{28}\) to \(10^{33}\) erg, a range of 4.3 orders of magnitude. The existence of the Pleiades flare shows that this distribution must continue to at least \(3 \times 10^{34}\), although we cannot determine whether it follows the same power-law slope or turns over. The predicted rate using the extrapolated 2M0335+23 FFD for the Pleiades superflare is 1.4 per year. The striking aspect of this power-law slope is that it agrees so well not only with stellar M6–M8 dwarfs, but also “inactive” M dwarf stars. It is also in excellent agreement with solar flares. Crosby et al. (1993) found that \(\alpha \approx 1.5\) for solar hard-X ray flares over three orders of magnitude. Aschwanden et al. (2000) argue that solar flares follow a power low slope with \(\alpha = 1.8\) over the range \(10^{24} - 10^{32}\) erg. Power-law slopes near this value are explained by self-organized criticality models (Lu & Hamilton 1991; Aschwanden et al. 2016) where flares are due to “avalanches” of many small magnetic reconnection events. 2M0355+11 may be at a temperature \((1480 \text{ K})\) below which fast magnetic reconnection events are no longer possible.

While the slopes (\(\alpha\)) are consistent between the brown dwarfs, the Sun, and other stars, the overall normalization of the flare rate (\(\phi\)) is very different. Flares on 2M0335+23 are much less frequent than in the rapidly rotating M4 dwarf GJ 1243 (Silverberg et al. 2016), comparable to “inactive” M dwarfs studied by Hawley et al. (2014), and more frequent than in the Sun. It is perhaps most interesting to compare to the L1 dwarf W1906+40. At an energy of \(10^{32}\) erg, flares are 3–4 times as frequent on 2M0335+23 as on W1906+40. However, 2M0335+23 is 13 times more luminous than W1906+40, so
despite its higher temperature, it is less efficient at converting its energy into flares; it also has seven times the surface area of W1906+40 so the flare rate per unit area is lower. It is intriguing that in the Reiners & Christensen (2010) theory, W1906+40’s predicted magnetic field is 3.1 kG, 40% stronger than that of 2M0335+23.

If we compute the total power in 2M0335+24 white light flares as the integral of $EdN$ from the solar microflare energy of $10^{23}$ erg to the observed superflare energy of $2.6 \times 10^{34}$ erg using the 2M0335+23 FFD fit, we find $\log L_{\text{WLF}}/L_{\text{bol}} = -4.2$. A more conservative upper limit of $10^{33}$, and lower limit of $5 \times 10^{28}$ erg still give $\log L_{\text{WLF}}/L_{\text{bol}} = -4.7$.

4.3. The Pleiades Brown Dwarf Superflare

With an energy of $2.6 \times 10^{34}$ erg, the CFHT-PL-17 flare event is comparable to superflares observed in Kepler G, K, and M stars (Candela et al. 2014), though below the mean observed superflare energy (Davenport 2016). It is helpful to consider the flare in terms of the observed peak absolute $M_{\text{bp}} = 10.3$ (long cadence) or $-8.7$ (short cadence). If this brown dwarf were an unresolved companion to an A star ($M_{\text{bp}} \approx 0$) or F dwarf ($M_{\text{bp}} \approx 2.5$) the flare would be a detectable event with Kepler. However, the flare rates seen in some A and F stars by Balona (2012) seem to be too high to be explained by brown dwarf companions, since they re-occur on timescales of 1–120 days whereas we expect less than one per year due to a brown dwarf. X-ray-triggered events have revealed that even more energetic superflares occur in young M dwarfs such as the ~30 Myr old M dwarf binary DG CVn (Osten et al. 2016). For comparison with other ultracool dwarfs, this superflare has more energy than the L1 dwarf superflare we reported in Paper I but less than the ASASAN-16ae L0 dwarf superflare (Schmidt et al. 2016).

As noted above, the extrapolated flare rate of 2M0335+23 suggests a superflare only ~1.4 times per year. We find that there are nine well-resolved Pleiades brown dwarfs in the spectral type range M6-M9 Campaign 4 for which we would have detected a similar superflare. The combined superflare rate of these nine brown dwarfs is ~1.7 times per year. This suggests that the superflare may be understood as the high-energy tail of the white light flare power-law distribution. However, Rubenstein & Schaefer (2000) suggested superflares in solar-type stars may be the result of interactions with a planetary companion, and we have no information about whether CFHT-PL-17 may have a lower-mass brown dwarf or exoplanet companion. We see no reason to invoke interactions with a substellar companion to explain the white light flares in either 2M0335+23 or CFHT-PL-17.

4.4. Complex Flares: Is Sympathetic Flaring at Work?

The two 2M0335+23 complex flares (Figure 2, Table 2) are very well described as the sum of two individual flares that follow the template, and we assume throughout this section that they are occurring on 2M0335+23 rather than an unknown companion. The time separation is 14.6 min for the flare on mission day 2240 and 9.2 min for the flare on mission day 2287. A third possible example of a complex flare occurs on mission day 2258, with a time separation of about 8 min. However, in the third case, the noise level is large enough that it is not altogether clear that two individual flares can be reliably identified. Thus, among the 22 flares illustrated in Figure 2, we can confidently state that about 10% exhibit the occurrence of two flares within a time interval shorter than 20 min.

Flares which occur within a short time interval of each other may belong to the class of “sympathetic flares” (SFs). By definition, SFs are related to each other in the sense that a disturbance (of a kind that we will discuss below) generated by the first flare propagates to another active region and triggers a flare there. However, a “short” time interval between flares is not necessarily an indication of an SF. In fact, it may be difficult to identify with confidence a bona fide SF in certain stars. For example, a very active flare star may have multiple flares occurring randomly in multiple active regions within short time intervals, and these flares may have little or physical relationship to one another. Is there a way to distinguish between unrelated flares and SFs? We suggest that one possible approach may be to consider the ratio of (i) the time interval $T$ between two particular flares, and (ii) the mean time interval $T(m)$ between flares averaged over the length of the entire observing period.

For example, the M4 flare star GJ 1243 (Davenport et al. 2014) was observed by Kepler for a period of 11 months, during which 6107 “unique events” were identified as flares. This star has an average of 18–19 flares per day, i.e., $T(m) = 75–80$ min. An example of a “complex flare” is illustrated by Davenport et al. (2014) in their Figure 6, which spans an interval of 3.6 hr: seven template flares are required to produce a good fit to the light curve. The average time interval between the template flares in this case is $T = 31$ min. This is already shorter than $T(m)$ by a factor of 2, and might therefore suggest that SFs could be at work. A fortiori, if we exclude one outlier flare at late times (with a peak at abscissa 549.865 days), inspection of their Figure 6 suggests that five template flares occurred on GJ 1243 within a time interval of only 75 min, i.e., $T = 15$ min. This is 5–6 times shorter than $T(m)$, again suggestive of SFs.

In contrast to the active flare star GJ 1243, when we return to considering the object of interest to us here (2M0335+23), we find that the flares in Figure 2 were observed over a 66 day interval. This means that, with 21 flares in our sample, the mean interval between flares is $T(m) = 3$ days. The fact that we have identified two (or possibly three) pairs of flares separated by only 20 min means that our pairs of flares have time separations $T$ which are shorter than 0.01$T(m)$. As a result, while we may assert that neighboring flares on 2M0335 are probably randomly related if they are separated by 3 days or more, it is much more difficult to make such an assertion for flares which are separated by less than 1% of $T(m)$. It seems more likely to consider the possibility that two flares which are separated by only 1% of $T(m)$ are physically related to each other. Specifically, is it possible that we are observing pairs of SF in 2M0335+23?

In the Sun, the SF possibility was subject to opposing claims in the 1930s based on optical data (Richardson 1937; Waldmeier 1938). Conflicting claims for the existence (or non-existence) of SFs surfaced again in the 1970s, based on radio and X-ray data (Fritzova-Svestkova et al. 1976: hereafter FCS). Based on X-ray data, FCS reported on the absence of significant evidence for SFs except in one subset of their data: active regions which were closer to each other than a critical distance exhibited a 3.4σ increase in the occurrence of “short” time intervals between flares. Coincidentally, FCS
defined “short” as being <20 min, i.e., the same interval as we mentioned above in connection with flares on 2M0335+23. However, FCS seemed suspicious about even the one SF case they had detected because they could not identify “any mode of propagation of a triggering agent in the solar atmosphere.”

In the case of stars, Oskanyan & Terebizh (1971; OT) analyzed the time intervals between successive flares in YZ CMi and UV Cet and found that the intervals in general followed a Poisson distribution. However, in UV Cet, there exist certain “sequences of closely spaced flares whose probability of occurrence is very small in the case of a Poisson process.” In one case, seven flares occurred in 5.4 min, and on each of two separate occasions, three flares were observed within a 2 min interval. OT demonstrated that such small intervals of time between flares are highly improbable in the context of the overall Poisson distribution.

In the case of the same flare star as discussed by OT, Haupt & Schlosser (1974; HS) reported on an independent study of the time intervals between flares on UV Cet. In the course of 26 hr of observing, they detected 94 flares. Thus, they obtained $T (m) = 17$ min as the average time between flares. However, when they examined the distribution of time intervals between individual flares, the intervals ranged up to as long as 110 min. A Poisson distribution was found to fit the flare interval data at the 98% confidence level with one proviso: only intervals larger than 4 min were included. At intervals shorter than this, there is a large spike in the distribution: 38 of the 94 flares were found to have $T \leq 4$ min. This excess at short times is far above what the Poisson distribution predicts. HS cited OT as having also noted this excess at short times. But then, with regard to the excess at short times, HS make the following statement (which has no explicit analog in OT): “This might be due to triggering of the second flare by the first, like sympathetic flares on the Sun.”

A possible triggering agent for SFs in the Sun was suggested by Uchida (1968): a fast-mode magnetohydrodynamic (MHD) wave/shock which is launched into the corona by certain flares. The idea is that as the wave/shock propagates through the corona, it may encounter a second active region: in that case, the wave/shock may perturb the second active region in such a way that a “sympathetic” flare occurs in that active region. Evidence for disturbances propagating away from certain flare sites was at first based solely on chromospheric data, where a “Moreton wave” was observed sweeping across the chromosphere. An observational breakthrough as regards a triggering agent for SFs occurred with the launch of SOHO in 1995, when the extreme-ultraviolet (EUV) Imaging Telescope (EIT) detected waves which propagate through large distances in the solar corona following certain events. The waves are referred to variously as “EIT waves” or “EUV waves.” The waves were first interpreted as fast-mode MHD waves driven either by an erupting coronal mass ejection (CME) or as a blast wave driven by the energy release in a flare. The earliest data indicated that EUV waves propagate at speeds of 200–500 km s$^{-1}$ in the solar corona (Klassen et al. 2000), but speeds as large as 1400 km s$^{-1}$ have been reported (Nitta et al. 2013). An extensive survey of multiple theories which have been proposed to explain EUV waves (Long et al. 2016) has concluded that the waves in the Sun are “best described as fast-mode large-amplitude waves or shocks that are initially driven by the impulsive expansion of an erupting CME in the low corona.”

In the case of stellar (and brown dwarf) flares, is it possible that we might rely on solar-like phenomena to understand SFs? Flares on stars involve magnetic energy release, so to the extent that a stellar flare contributes to the launch of a blast wave in the corona (analogous to the Sun), we may expect that flare-induced EUV waves could contribute to stellar SFs. What about EUV waves generated by CMEs? Can we count on those to occur in flare stars and serve to launch EUV waves to help generate SFs? Although flares and CMEs in the Sun both involve release of magnetic energy, they do not always occur together: one can occur without the other, depending on local details of the parent active region. We note that at least one detection of a stellar CME has been reported from an active K dwarf which is known to be a flare star (Bond et al. 2001).

Let us examine the hypothesis that the two complex flares which we have detected in 2M0335+23 involve SFs which are triggered by the equivalent of an EUV wave. In this context, the maximum speed of the wave would be obtained if the two active regions which are involved in the individual flares were located at antipodal points on the surface of 2M0335+23, at a distance $\pi R$ from each other. Inserting the radius $R$ of 2M0335+23, and inserting time delays of 14.6 and 9.2 min, the SF hypothesis leads to $v (EUV) < 600$ and 950 km s$^{-1}$. Such values are well within the range of EUV wave speeds that have been reported in the solar corona. With fast-mode speeds determined mainly by the Alfvén speed (which greatly exceeds the thermal speed of order 100–200 km s$^{-1}$ in a 1–2 MK corona), our SF interpretation suggests that Alfvén speeds in the corona of 2M0335+23 may not differ greatly from those in the solar corona. In the latter, a map of coronal Alfvén speeds reported by Susino et al. (2015) spans a range from 500 to 900 km s$^{-1}$ at essentially all latitudes within a radial distance of five solar radii.

4.5. Complex Flares: Does the Weakness of the Second Flare Contain Physical Information?

We note that for the complex flares in Figure 2, when the tail of the first light curve is subtracted from the second flare, the amplitude at the peak of the second flare is smaller than that at the peak of the first. We ask: Is this “weaker secondary” a common feature of complex flares?

To address this, we consider some flare data which were recorded in different settings.

1. A large homogeneous sample of X-ray flares which were recorded by Chandra in the Orion Ultradeep Project (Getman et al. 2008). In their study of the 216 brightest flares from 161 pre-main sequence stars, eight events were classified as double flares, i.e., they looked like two overlapped typical flares. By subtracting off the tail of the first flare in each case, we evaluated the ratio of peak 2 to peak 1, and found the following values: 0.3, 0.4, 0.2, 0.5, 1.1, 0.2, 0.3, and 0.1. Thus, in seven out of eight cases, the sympathetic flare had a smaller amplitude than the original flare.

2. Optical data (in the $r$ band) for stars in the intermediate-age cluster M37 (0.55 Gyr) resulted in detection of several hundred flares from cluster members (Chang et al. 2015a, 2015b). Chang et al. (2015b) drew attention to the result that their algorithm often detects secondary flares which occur during the decay of a much larger flare. Visual inspection of Figure 2 in Chang et al. (2015b) and
Figures 17 and 18 in Chang et al. (2015a) suggests that as many as eight or nine secondary flares can be identified among the plotted light curves of 23 stars: in all cases but one, the flare which occurred later in time was smaller in amplitude than the first flare.

3. A small sample (15–20) of light curves in a variety of visible and near-UV wavelengths from a number of solar neighborhood flare stars was presented by Gershberg (2005, p. 195) Secondary flares can be identified in at least five cases, and in all cases the flare which occurred later in time had a smaller peak intensity. These examples suggest that, no matter which wavelength range we examine, the flare which occurs later in time (the “secondary”) in a “close double” has (in most cases) a smaller amplitude than the flare which occurs earlier. We believe that this is a feature which contains information related to one of the key physical processes involved in sympathetic flaring.

How might this “weaker secondary” behavior be understood in the context of the SF explanation proposed above (i.e., the SF is triggered by a fast-mode MHD wave)? We suggest that it may be understood in terms of wave refraction. When fast-mode MHD waves propagate through an inhomogeneous medium, the compressive nature of the waves has the effect that they are refracted away from regions of high Alfvén speed ($v_A$), and are refracted into regions where $v_A$ is small (Uchida 1968). (Alfvén waves, lacking compression, refract differently.) Tests of Uchida’s predictions have been provided by observations (e.g., Shen et al. 2013) and modeling (e.g., Steinolfson & Mullan 1980; Jin et al. 2016) of fast-mode waves propagating through a variety of structures in the solar corona. However, the tests mentioned in the preceding sentence were based on indirect inferences of the $v_A$ value in different regions of the Sun. For more reliable tests of Uchida’s theory, it is preferable to consider a medium where in situ measurements of field strength and ion density can be made directly: in such a medium, the local value of $v_A$ can be calculated, various wave modes can be distinguished (fast MHD, slow MHD, Alfvénic), and Uchida’s predictions can be tested directly. The solar wind is one such medium. In the solar wind at a radial distance of about 1 au, data from the ACE satellite have been used to demonstrate that fast-mode waves are indeed depleted in high-$v_A$ regions (Smith et al. 2001), and fast-mode waves are indeed enhanced in regions of low $v_A$ (Mullan et al. 2003).

Now let us consider how these results might find an application in SFs in low-mass stars. Suppose an initial flare is triggered (somehow) in a certain active region (AR), thereby launching a fast-mode EUV wave with a certain speed: this will be related to the $v_A$ value in the AR where the flare was initiated. Suppose there are two other ARs on the surface of the star, AR-A with large $v_A$, and AR-B with small $v_A$. What happens when the EUV wave approaches AR-A? The fast-mode wave will be refracted away from AR-A because of the locally large $v_A$, and will be unable to penetrate into it. Therefore, an SF is unlikely to occur in AR-A. But in the case of AR-B, the fast-mode wave will be refracted into the AR, thereby having a chance to perturb the plasma inside AR-B, perhaps enough to initiate a flare. In this scenario, an SF is more likely to occur in an AR with a small $v_A$ or, in the terminology of Jin et al. (2016), the “impact” of the wave on AR-B (with its lower $v_A$) would be larger. What might cause the $v_A$ value in AR-B to be smaller? It could be either a weaker field or higher density, or both. In cases where the field is weaker, we expect that (other things being equal) a flare in such an AR will have (in general) a smaller total energy. Thus the flare originating in AR-B (where the “impact” of the fast-mode wave is largest) will be “weaker,” and is expected to have a smaller peak amplitude. If this is a correct interpretation of SFs in stars, then the phenomenon of the “weaker secondary” may provide an observational signature of the physics of refraction of fast-mode MHD waves in the inhomogeneous corona of a flare star.

5. Conclusions

White light flares on a young (24 Myr) M7-type brown dwarf are similar in most respects to stellar M dwarf flares, including their light curves, power-law flare frequency distribution, and sympathetic flaring. Adding a flare on a Pleiades brown dwarf, we see that these flares extend up to at least $2.6 \times 10^{34}$ erg. However, we observe no white light flares on the L5-type brown dwarf despite its known young age and rapid rotation. Since there is overwhelming observational and theoretical evidence that magnetic fields exist on L- and T-type brown dwarfs, we conclude that the change in flare rates is direct evidence that fast magnetic reconnection is suppressed or forbidden at temperatures $\sim1500$ K. In this work, we have studied brown dwarfs of known age. In our next paper, we will measure the white light flare rates of a sample of field late-M and -L dwarfs and investigate their dependence on age, rotation, effective temperature, and other observable properties.

We thank James Davenport and Rachel Osten for discussions of stellar flares, Jonathan Gagné and Jackie Faherty for discussions of moving groups, Mike Liu and Conard Dahn for comments on the preprint, and the anonymous referee and statistical consultant for suggestions. This paper includes data collected by the Kepler mission. Funding for the Kepler mission is provided by the NASA Science Mission directorate. The material is based upon work supported by NASA under award Nos. NNX15AV64G, NNX16AE55G, and NNX16AJ22G. A.J.B. acknowledges funding support from the National Science Foundation under award No. AST-1517177. Some of the data presented in this paper were obtained from the Mikulski Archive for Space Telescopes (MAST). STScI is operated by the Association of Universities for Research in Astronomy, Inc., under NASA contract NAS5-26555. Support for MAST for non-HST data is provided by the NASA Office of Science Space via grant NNX09AF08G and by other grants and contracts. Some of the data presented herein were obtained at the W.M. Keck Observatory, which is operated as a scientific partnership among the California Institute of Technology, the University of California and the National Aeronautics and Space Administration. The Observatory was made possible by the generous financial support of the W.M. Keck Foundation. This research has made use of NASA’s Astrophysics Data System, the VizieR catalog access tool, CDS, Strasbourg, France, and the NASA/IPAC Infrared Science Archive, which is operated by the Jet Propulsion Laboratory, California Institute of Technology, under contract with NASA. We have also made use of the List of M6-M9 Dwarfs maintained by Jonathan Gagné.

Software: IRAF, AstroPy (Astropy Collaboration et al. 2013), photutils, emcee (Foreman-Mackey et al. 2013), PyKE (Still & Barclay 2012), APLpy, powerlaw (Alstott et al. 2014).

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