GRB/GW ASSOCIATION: LONG-SHORT GRB CANDIDATES, TIME-LAG, MEASURING GRAVITATIONAL WAVE VELOCITY AND TESTING EINSTEIN’S EQUIVALENCE PRINCIPLE

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ABSTRACT

Short duration GRBs (SGRBs) are widely believed to be powered by the mergers of compact binaries, like binary neutron stars or possibly neutron star-black hole binaries. Though the prospect of detecting SGRBs with gravitational wave (GW) signals by the advanced LIGO/VIRGO network is promising, no known SGRB has been found within the expected advanced LIGO/VIRGO sensitivity range for binary neutron star system.

We find, however, that the two long-short GRBs (GRB 060505 and GRB 060614) may be within the horizon of advanced GW detectors. In the upcoming era of GW astronomy, the merger origin of some long-short GRBs, as favored by the macronova signature displayed in GRB 060614, can be unambiguously tested. The model-dependent time-lags between the merger and the onset of the prompt emission of GRB are estimated. The comparison of such time-lags between model prediction to the real data expected in the era of the GW astronomy would be helpful in revealing the physical processes taking place at the central engine (including the launch of the relativistic outflow, the emergence of the outflow from the dense material ejected during the merger and the radiation of gamma-rays). We also show that the speed of GW, with or without a simultaneous detection of macronova, can be directly measured an accuracy of \( \sim 3 \times 10^{-8} \) cm s\(^{-1}\) or even better in the advanced LIGO/VIRGO era.

Subject headings: gamma-ray burst; general—stars: black holes—stars: neutron—binaries: general

1. INTRODUCTION

The coalescence of a binary compact system (either a neutron-star (NS) binary or a stellar-mass black hole (BH) and NS binary) has been widely suggested to account for short-duration gamma-ray burst (SGRB) events (Eichler et al. 1989, Narayan et al. 1992, Nakar 2007, Berger 2014) that lasted typically shorter than 2 seconds in soft gamma-ray band (Kouveliotou et al. 1993). Since 2006, it had been suspected that the compact object mergers could also produce the so-called long-short GRBs (also known as the supernova-less long GRBs which are apparently long-lasting but do not show any signal of supernovae down to very stringent limits) which share some properties of both long- and short-duration GRBs (Gehrels et al. 2006, Della Valle et al. 2006, Gal-Yam et al. 2006, Zhang et al. 2007). The compact binary coalescence (CBC) is generally expected to be strong gravitational wave (GW) radiation source and are prime target for some gravitational detectors like advanced LIGO/VIRGO (Abadie et al. 2015, Acernese et al. 2015, Belczynski et al. 2016, see also the latest LSC-Virgo white paper at https://dcc.ligo.org/LIGO-T1400054/public). On September 14, 2015 the two detectors of the Laser Interferometer Gravitational-Wave Observatory (LIGO) simultaneously detected a transient gravitational-wave signal from the merger of two black holes (GW150914, Abbott et al. 2016). GW150914 is the first direct detection of gravitational waves and the first identification of a binary black hole merger (Abbott et al. 2016). Surprisingly, the Fermi Gamma-ray Burst Monitor (GBM) observations at the time of GW150914 claimed a detection of a weak gamma-ray transient (i.e., GBM transient 150914) 0.4 s after GW150914 with a false alarm probability of 0.0022 (Connaughton et al. 2016). If true, this is the first GW/SGRB association (see however Savchenko et al. 2016 for some arguments). Li et al. (2016) compared GBM transient 150914 with other SGRBs and found that such an event is remarkably different in the prompt emission properties. The binary black hole merger origin as well as its “distinguished” prompt emission property suggest that GW150914/GBM transient 150914 is not a typical GW/SGRB association.

In the absence of successful detection of the gravitational radiation triggered by a “normal” (S)GRB (Abadie et al. 2012, Aasi et al. 2014, 2016), a “smoking-gun” signature for the compact-binary origin would be the detection of the so-called Li-Paczynski macronova (also called a kilonova), which is a near-infrared/optical transient powered by the radioactive decay of \( r \)-process material synthesized in the ejecta that is launched during the merger event (e.g., Li & Paczynski 1998, Kulkarni 2005, Metzger et al. 2016, Barnes & Kasen 2013). The identification of macronova candidates in the afterglows of the canonical short event GRB 130603B (Tanvir et al. 2013, Berger et al. 2013), the long-short burst GRB 060614 (Yang et al. 2013, Jin et al. 2015) and the short event with extended X-ray emission GRB 050709 (Jin et al. 2016) are strongly in support of the CBC origin of some GRBs. A conservative estimate of the macronova rate favors a promising detection prospect of the GW radiation by the (upcoming) advanced LIGO detectors (Jin et al. 2015). We anticipate that in the near future many compact-object-merger driven GW sources would be detected (Abadie et al. 2016) and a small fraction of such events would be accompanied by supernova-less GRBs (including both the short and long-short events).
The observation of a “nearby” supernova-less GRB provides a reliable estimate of the time, sky location and distance of a potential binary merger signal. This significantly reduces the parameter space of a follow-up GW search and consequently could be used to reduce the effective detection threshold and effectively increase the detectors’ sensitivity and their detection rate (e.g., Kochanek & Piran 1993; Finn et al. 1999; Harry & Fairhurst 2011; Kelley et al. 2013; Nissanke et al. 2013; Dietz et al. 2013; Williamson et al. 2014; Clark et al. 2015). In this work we examine whether some SGRBs and/or long-short GRBs are within the horizon of the advanced LIGO/VIRGO network and discuss the model-dependent time lag between the coalescence and GRBs.

This work is structured as follows: In Sec. 2 we discuss/summarize the prospect of detecting GW-associated GRBs in the era of advanced LIGO/VIRGO and examine whether any recent GRBs (either SGRBs or long-short GRBs) are within the horizon of the advanced LIGO/VIRGO network. In Sec. 3 the model-dependent time lags between the merger and GRBs are presented and the possibility of revealing the nature of merger remnants with such time delays is discussed. The expected progress in measuring the speed of GW with the future data are investigated in Sec. 4. Our results and discussion are presented in Sec. 5.

2. The prospects of detecting GW signal associated SGRBs and long-short GRBs

2.1. The prospect of detecting SGRBs associated with GW signals

The strategy of the targeted search for GWs associated with short GRBs has been extensively discussed in Harry & Fairhurst (2011) and Williamson et al. (2014). The prospect of detecting SGRBs with GW signals has also been widely estimated in the literature (e.g., Williamson et al. 2014; Wanderman & Piran 2015; Clark et al. 2015) and in this subsection we simply summarize their main conclusions.

2.1.1. BNS mergers

The sensitive distance can be approximated as (Clark et al. 2015)

\[ D_{\text{SNS}} \approx 400 \text{ Mpc} \left( \frac{9}{\rho_*} \right), \]  

where \( \rho_* \) is the signal-to-noise of the GW signal. When the advanced LIGO/VIRGO network has reached its full sensitivity, with the ‘local’ SGRB detection rate of \( 4 \pm 2 \text{ Gpc}^{-3} \text{ yr}^{-1} \) (Wanderman & Piran 2015), the detection rate of the GW signal associated SGRB for a full sky \( \gamma \)-ray monitor is estimated as

\[ \mathcal{R}_{\text{full sky}}(\rho_* = 9) \approx 1 \pm 0.5 \text{ yr}^{-1}, \]  

where all SGRBs are assumed to originate from BNS mergers. Such an assumption seems reasonable since the BH–NS merger rate is generally expected to be just \( 1/10 \) times that of the BNS merger rate (Abadie et al. 2010). Please note that the LIGO/Virgo network can boost gravitational wave detection rates by exploiting the mass distribution of neutron stars within BNS system, and for searches with detected electromagnetic counterparts the detection rate may increase of 60% (Bartos & Marka 2015).

2.1.2. BH-NS mergers

No neutron star-black hole (NS-BH) binaries have not been directly observed yet (Lattimer 2012) but indirect evidence for NS-BH merger has been suggested in the macronova modeling (Yang et al. 2015; Jin et al. 2015). In a systematic analysis of the BH mass distribution based on 35 X-ray binaries, Farr et al. (2011) found strong evidence for a mass gap between the most massive neutron stars and the least massive black holes, confirming the results of Bailyn et al. (1998) and Ozel et al. (2010). For the low-mass systems (combined sample of systems), they found a black hole mass distribution whose 1% quantile lies above \( 4.3 M_\odot (4.5 M_\odot) \) with 90% confidence. The typical NS-BH binary systems are expected to have a mass ratio of \( 1 : 4 \), for which the sensitive distance of the aLIGO/AdV network can be estimated as

\[ D_{\text{NS-BH}} \approx 690 \text{ Mpc} \left( \frac{9}{\rho_*} \right). \]  

If \( \sim 1/5 \) of short and long-short GRBs are produced by NS-BH mergers, while aLIGO/AdV are more sensitive to the heavier NS-BH system, we expect around half of the CBC events might have an EM counterpart has an origin of NS-BH mergers.

As an optimistic estimate (i.e., supposing most nearby SGRBs can be observed by Fermi GBM-like detectors), in 10 years of full run of aLIGO/AdV network \( 10 - 20 \) GW-associated SGRBs are expected and possibly one half of them may have an NS-BH merger origin. The statistical study of such a sample, though still limited, may shed valuable light on the physical processes taking place at the central engine (see Sec. 4 for the details) and possibly also the fundamental physics (see Sec. 4 for the details). In addition to SGRBs, some supernova-less long GRBs may also have a compact object merger origin and the detection rate of merger events will increase.

2.2. “Supernova-less” GRBs within the sensitivity distance of advanced LIGO/VIRGO network

As shown in Sec. 2.1 the detection prospect of GW-associated SGRBs is promising for the advanced LIGO/VIRGO network. The nearest short burst is GRB 061201. It is measured to have a redshift of \( z = 0.111 \) (Berger 2014, see however D’Avanzo et al. (2014) for the uncertainty), or a distance of 520 Mpc, which is larger than \( D_{\text{BNS}}(\rho_* = 9) \). Note that most SGRBs are expected to be powered by BNS mergers, hence no single SGRB has been found within the averaged sensitive distance of the advanced LIGO/VIRGO network (Williamson et al. 2014; Wanderman & Piran 2015). Such a result is somewhat disappointing though not in significant tension with the expectation (see eq. (4)). To better explore the situation, in this work we also take into account all “nearby” (i.e., \( z < 0.3 \)) supernova-less long GRBs, including XRF 040701 (X-ray flash, Soderberg et al. 2005), GRB 060505 and GRB 060614 (Fynbo et al. 2006). Please note that actually some “SGRBs” with the so-called extended emission can also be classified as supernova-less long GRBs, but such events have also been included in previous GW/SGRB association studies. Below we focus on the “traditional” long-short GRBs and introduce them in some details.

XRF 040701 was localized by the Wide-Field X-Ray Monitor on board the High Energy Transient Explorer (HETE-2) on 2004 July 1.542 UT. It is characterized by the very low peak frequency (i.e., <6 keV) of the prompt emission. Soderberg...
et al. (2005)’s foreground extinction-corrected HST detection limit is \( \approx 6 \) mag fainter than SN 1998bw, the archetypal hypernova that accompanied long GRBs (Galama et al. 1998), at a redshift of \( z = 0.21 \). The analysis of the X-ray afterglow spectra reveals that the rest-frame host galaxy extinction is constrained to \( A_{V,host} < 2.8 \) mag, suggesting that the associated supernova, if there was, should be at least \( \sim 3.2 \) mag fainter than SN 1998bw (Soderberg et al. 2005). Due to the lack of the sufficient multi-wavelength afterglow data, the “absence” of a bright supernova associated with XRF 040701 did not attract wide attention. The situation changed dramatically when the supernovae associated with GRB 060505 and GRB 060614 had not been detected down to limits hundreds of times fainter than SN 1998bw (Fynbo et al. 2006). Particularly, GRB 060614, a bright burst with a duration of \( \sim 102 \) s at a redshift of 0.125, had dense followup observations with Very Large Telescope and Hubble Space Telescope. The physical origin (either a peculiar collapsar or a compact object merger) of GRB 060614 was debated over years (e.g., Fynbo et al. 2006, Gehrels et al. 2006, Della Valle et al. 2006, Gal-Yam et al. 2006, Zhang et al. 2007). The re-analysis of the optical afterglow emission of GRB 060614 found significant excess components in multi-wavelength photometric observations, which can be reasonably interpreted as a Li-Paczynski macronova that powered by the radioactive decay of debris following an NS-BH merger while the weak supernova model does not work (Yang et al. 2013, Jin et al. 2013). As summarized in Xu et al. (2009), the origin of GRB 060614 at a redshift of \( z = 0.089 \) is less clear. The properties of its host galaxy seems to be consistent with that expected for the long-duration GRBs (Thöne et al. 2008) but GRB 060505 is an outlier of the so-called Amati relation that holds for long GRBs (Amati et al. 2007). The HST observations at \( t \sim 14 \) days after the burst did not find optical emission down to a limiting AB magnitude of 27.3\(^{m}\) in F814W band and 27.1\(^{m}\) in F475W band (Olek et al. 2007). Such stringent limits are strongly at odds with the collapsar model but can be well consistent with the BNS merger model as long as the \( r \)-process ejecta has a mass \(< 10^{-7} \) M\(_{\odot}\) (Jin et al. 2016).

It may be still a bit early to conclude that all “nearby supernova-less” long GRBs (i.e., “long-short GRBs”) are from compact object binary mergers. The successful identification of a macronova signal in the long-short event GRB 060614, nevertheless, renders such a possibility more attractive than before. If the NS-BH merger model for GRB 060614 is correct, the luminosity distance of this event is \( D_L \approx 576 \) Mpc, which is smaller than \( D_{L,\text{BNS}} \) as long as \( \rho_s \leq 10.8 \) (see eq. [3]). For GRB 060505, the redshift \( z = 0.089 \) corresponds to a luminosity distance \( D_L \approx 400 \) Mpc, which almost equals to \( D_{L,\text{BNS}} \) for \( \rho_s = 9 \) (see eq. [1]). Intriguingly, among the supernova-less and short events detected so far (note that the GBM transient 150914 is still uncertain), the long-short burst GRB 060505 and GRB 060614 are the only candidates that might yield detectable GW signal for the advanced LIGO/VIRGO network (see Fig.1).

The presence of two Swift GRB candidates within the averaged sensitivity distance of the advanced LIGO/VIRGO network for \( \rho_s \geq 9 \) is indeed very encouraging for the ongoing GW experiments. On the other hand, if the supernova-less long-duration XRFs/GRBs were from a peculiar kind of collapsar (which is very unlikely to be the case for GRB 060614), we can verify it with the non-detection of GW signal. Therefore we suggest that the supernova-less long-duration XRFs/GRBs are one of prime targets for advanced LIGO/VIRGO network and the nature of such a kind of “mysterious” events would be unambiguously pinned down in the era of GW astronomy.

3. MODEL-DEPENDENT ESTIMATES OF TIME LAG BETWEEN BINARY COALESCENCE AND GRB ONSET

Though extensively studied, so far the launching, acceleration and energy dissipation of the GRB ejecta are still heavily debated (see Zhang 2014, for a dedicated review). Instead of carrying out advanced study of a specific model, in this section we adopt some widely-discussed scenarios and present our model-dependent estimates of time lag between GW coalescence time and GRB onset (i.e., \( \Delta_{\text{GW-GRB}} \)) and examine a statistical study of \( \Delta_{\text{GW-GRB}} \) could help us to better understand the physical processes taking place at the central engine.

In general, \( \Delta_{\text{GW-GRB}} \) can be divided into two parts. One is the time delay between the merger time, which could be estimated by analyzing the GW data (e.g., Fairhurst 2011, Veitch et al. 2013), and the successful launch of the ultra-relativistic ejecta (i.e., \( \Delta_{\text{laun}} \)). The other is the time delay between the launch of the ultra-relativistic ejecta and the onset of the gamma-ray emission (i.e., \( \Delta_{\text{em}} \)). Below we examine \( \Delta_{\text{laun}} \) and \( \Delta_{\text{em}} \) separately under different models and then get
the corresponding estimate of
\[ \Delta t_{\text{GW-GRB}} = \Delta t_{\text{laun}} + \Delta t_{\text{enm}}. \]

Notice that we are using the coalescence time, when the GW signal spikes, as a proxy to the merger moment. One might reasonably argue that these two are not identical, but as the binary system evolve very rapidly towards the merger, they should not differ by more than a couple of rotations around the merger. For BNS systems the merger frequency is around 1000Hz so the difference in time can not exceed \( \sim 1 \text{ms} \) (Fairhurst, 2011; Pirret, 2014).

In this work we focus on the most widely-adopted hypothesis that the SGRBs were powered quickly after the merger (i.e., \( \Delta t_{\text{GW-GRB}} < 10 \text{ s} \)). However notice that a small amount of SGRBs seem to have precursor emission and the precursors are likely from the same central engine activity as the main bursts (Charisi et al., 2015). In the binary merger scenario, the merger may likely happened before the precursor. If so, the time-lag between the GW signal and the SGRB/long-short GRB can be long to \( \sim 100 \text{ s} \), which may label the lifetime of the supramassive neutron star formed in the merger or alternatively the fall-back accretion timescale of the fragmented part of the compact object. Rezzolla & Kumar (2015) argued that the BNS mergers might actually take place several hours before the SGRBs. The GW/GRB association observations can easily distinguish between such scenarios (i.e., \( \Delta t_{\text{GW-GRB}} < 10^2 - 10^4 \text{ s} \)) with and the short delay cases (i.e., \( \Delta t_{\text{GW-GRB}} < 10 \text{ s} \)), as shown in Tab. In a long time-lag between the GW and GRB signals, in principle, could also arise from the subluminal movement of the GW in the vacuum or its higher velocity than the photons in the gravitational potential. Such possibility can be precisely tested as long as a sample of GW/GRB association is established (see Sec.4.2 for the details).

3.1. \( \Delta t_{\text{laun}} \) expected in different merger scenarios

3.1.1. NS-NS mergers

The maximum gravitational mass of a cold non-rotating neutron star is known to be \( M_{\text{max}} > 2 M_{\odot} \) (Antoniadis et al., 2013) and the threshold for collapse of the merger-formed remnants into black holes can be estimated roughly as \( M_{\text{thres}} \approx 1.35 M_{\text{max}} \) (Shibata & Taniguchi, 2006). Hence a total gravitational mass \( \geq 2.7 M_{\odot} \) is likely required for prompt collapse to a black hole. Such massive neutron star binaries should just account for a small fraction of merger events if the mass distribution of “cosmic” neutron star binaries resembles what was observed in the Galaxy (see Lattimer, 2012, for a recent review). Hence usually we do not expect the prompt collapse of the merger-formed neutron stars. Instead the merger formed remnants are widely expected to be very massive neutron stars with strong differential rotation that can support against the collapse at least temporarily.

Such remnants are called the hypermassive neutron stars (HMNSs). The fate of the post-merger HMNSs is however uncertain, and is contingent on the mass limit for support of a hot, differentially rotating configuration (e.g., Baumgarte et al., 2000; Hotokezaka et al., 2013). Below we present the model-dependent estimates of the collapse time of the HMNSs which we regard as \( \Delta t_{\text{laun}} \). One exception would be presented in the last paragraph of this sub-subsection.

When \( M_{\text{max}} < M < M_{\text{thres}} \), various mechanisms could act to dissipate and/or transport energy and angular momentum, possibly inducing collapse after a delay which could range from tens of milliseconds to a few seconds (see Faber & Rasio, 2012 for a recent review). For instance, in the presence of strong magnetic field, the magnetic braking effect can effectively transfer the angular-momentum in a timescale \( \tau_{\text{br}} \approx R_{\text{d}}/V_{A} \sim 0.3 \text{ s} \) \( (R_{\text{d}}/10^6 \text{ cm})^{2} \rho/10^{15} \text{ g cm}^{-3} \tau_{\text{A}}(\varepsilon/0.3)(B/10^{12} \text{ G})^{-1} \), where \( V_{A} \) is the Alfvén’s velocity, \( R_{\text{d}} \), is the radius of the neutron star and \( \varepsilon \approx 0.3 \) is the expected strength ratio between the surface magnetic field \( B_{\text{s}} \) and the interior poloidal magnetic field (Sharp, 2000). Another mechanism is the magnetorotational instability (MRI), which generates turbulence in a magnetized rotating fluid body that amplifies the magnetic field and transfers angular momentum. In the presence of MRI, an effective viscosity is likely to be generated with the effective viscous parameter
\[ \nu_{\text{vis}} \sim \alpha_{\text{vis}} c_{s}^{5}/\Omega_{c}, \]
where \( \alpha_{\text{vis}} \) is the viscosity parameter, \( c_{s} \) is the sound velocity of the envelope of the HMNS and \( \Omega_{c} \) is the angular velocity of the core of the differentially-rotating neutron star (Balbus & Hawley, 1991). Thus, the viscous angular momentum transport time scale can be estimated as \( \tau_{\text{vis}} \sim \tau_{\text{acc}} \sim 10^{16} \text{s} \frac{M/10^{4} \text{M}_{\odot}}{R_{\text{d}}/10^{6} \text{cm}} \frac{(\alpha_{\text{vis}}/0.01)^{2}(c_{s}/0.1c)^{2}(\Omega_{c}/10^{4} \text{rad s}^{-1})^{-1}}{R_{\text{d}}/10^{6} \text{cm}} \) (Hotokezaka et al., 2013; Siegel et al., 2013). A reasonable estimate of the termination timescale of the differential rotation is \( \tau_{\text{diff}} = \min[(\tau_{\text{acc}}, \tau_{\text{vis}})] \approx 0.1 \text{s} \), after which the HMNS is expected to collapse.

The situation is even less uncertain when both finite-temperature effects in the equation of state and neutrino emission of the central compact object have been taken into account. In the numerical simulations of the merger of binary neutron stars performed in full general relativity incorporating the finite-temperature effect and neutrino cooling, Sekiguchi et al., 2013 found that the effect of the thermal energy is significant and can increase \( M_{\text{max}} \) by a factor of \( 20\%-30\% \) for a high-temperature state with \( T \geq 20 \text MeV} \). Since they are not supported by differential rotation, the hypermassive remnants were predicted to be stable until neutrino cooling, with luminosity of \( \sim 3\times10^{53} \text{ erg s}^{-1} \), has removed the pressure support in \( \tau_{\text{thermal}} \sim 1 \text{s} \) (Sekiguchi et al., 2011).

For \( t < \tau_{\text{w}} \), a baryon-loaded wind is continuously ejected which would bound the bulk Lorentz factor of the jet to \( \Gamma_{w} \approx 5(\dot{L}_{\text{jet}}/10^{52} \text{erg s}^{-1})^{1/4}(M_{w}/10^{-5} \text{M}_{\odot} \text{ s}^{-1})^{-1} \), where \( \dot{L}_{\text{jet}} \) is the isotropic-equivalent luminosity of the jet, \( M_{w} \) is the mass loss rate via the wind and \( \tau_{w} \) is the wind duration (either \( \tau_{\text{diff}} \) or \( \tau_{\text{thermal}} \), depending on the mechanism that mainly supports against the collapse). Such a low \( \Gamma_{w} \) is too small to give rise to energetic GRB emission. Hence it is widely anticipated that no GRB is possible unless the neutrino-driven wind gets very weak or more realistically the neutron star has collapsed to a black hole. After the collapse of the HMNS, the earlier out-moving dense wind remains to hamper the advance of the jet, whose injection lifetime, \( \tau_{\text{jet}} \), is determined by the viscous timescale of the accretion disk (Lee et al., 2004). Murguia-Berthier et al., 2014 suggested that in the black hole central engine model for (short) GRBs, the black hole formation should occur promptly as any moderate delay at the hyper-massive neutron star stage would result in a choked jet. The argument that just the mergers with a remnant collapse within a timescale \( \tau_{\text{diff}} \sim 0.1 \text{s} \) can produce (short) GRBs may just hold in the scenario of energy extraction via neutrino mechanisms. The accretion timescale of the torus formed in binary neutron star mergers can be estimated as \( \tau_{\text{acc}} \sim 0.1 \text{s} (\alpha_{\text{vis}}/0.1)^{1/5} \) (Narayan et al., 2001).
In this case the central engine is a stellar mass black hole and the region along the spin axis of the black hole is likely cleaner than the case of NS-NS mergers. However, the joint effects of shocks during the disk circularization, instabilities at the disk/tail interface, and neutrino absorption unbinds a small amount (~ $10^{-4} M_\odot$) of material in the polar regions \cite{Foucart2015}. Over longer timescales, the neutrino-powered winds become active and eject material in the polar regions. Though the material is still negligible compared to the material ejected dynamically in the equatorial plane during the disruption of the neutron star, this ejecta could impact the formation of a relativistic jet \cite{Foucart2015}. Nevertheless, a few percents of the energy radiated in neutrinos is expected to be deposited in the region along the spin axis of the black hole through $\nu\bar{\nu}$ annihilations \cite{Setiawan2006, Janka1999}. The energy deposition at a rate $\sim 10^{51}$ erg s$^{-1}$ might also be able to power short $\gamma$-ray burst \cite{Foucart2014, Lee2007}.

As in the BNS merger scenario, the magnetic mechanism may be more promising in launching ultra-relativistic outflows and then giving rise to GRBs. In the recent high-resolution numerical-relativity simulations for the merger of BH-NS binaries that are subject to tidal disruption and subsequent formation of a massive accretion torus, the accretion torus formed quickly and the magnetic-field was amplified significantly due to the non-axisymmetric magnetorotational instability and magnetic winding \cite{Paschalidis2015, Kiuchi2015}. The amplification can yield $B \sim 10^{15}$ G at the BH poles in ~20 milliseconds after the merger and the

The expected time delay between the merger of the binary neutron stars and the launch of the ultra-relativistic GRB outflow can thus be approximately summarized as $\Delta t_{\text{fam,BNS}} \sim (0.01$ s, 0.1 s, 1 s) for (the prompt formation of black hole, differential rotation supported HMNS, thermal pressure supported HMNS), respectively. The minimum $\Delta t_{\text{fam,BNS}}$ is taken to be ~10 ms since the merger time is expected to be measured with an accuracy better than ~10 ms and the ultra-relativistic outflow may be launched promptly.

In the above discussion we assume that the short GRBs are produced when the HMNSs collapse into black holes. There is another possibility that the differentially-rotating NSs can eject a significant material towards the rotation axis which might also produce (short) GRBs. Such a scenario has attracted wide attention since the analysis of a good fraction of afterglow emission of \emph{Swift} short GRBs found possible evidence for the magnetor central engine \cite{Rowlinson2013}. One possible physical scenario is that the differentially rotating neutron star wraps the poloidal seed magnetic field into super-strong toroidal fields ($B_t \sim 10^{17}$ Gauss) that may emerge from the star through buoyancy and then generate GRBs via magnetic energy dissipation \cite{Kluza1998, Dai2006}. In this model $\Delta t_{\text{fam,BNS}}$ is expected to be the time needed to amplify the seed magnetic field to $B_t \sim 10^{17}$ Gauss, i.e., $\Delta t_{\text{fam,BNS}} \sim 5$ ms ($B_t/10^{17}$ Gauss/0.3)$B_{17}$ ($f_B/10^{15}$ G)$^{-1}$($\Delta \Omega/6000$ rad s$^{-1}$), where $\Delta \Omega \equiv 2\pi(1/P_c - 1/P_s)$, and $P_c$ and $P_s$ are the rotational periods of the differentially rotating internal part and main NS, respectively \cite{Kluza1998}. With the $B_t$ and the initial rotational periods of the magnetar central engine estimated in \cite{Rowlinson2013} we have $\Delta t_{\text{fam,BNS}} \sim 10 - 100$ ms.

3.1.2. NS-BH mergers

In the case of the central engine is a stellar mass black hole and the region along the spin axis of the black hole is likely cleaner than the case of NS-NS mergers. However, the joint effects of shocks during the disk circularization, instabilities at the disk/tail interface, and neutrino absorption unbinds a small amount (~ $10^{-4} M_\odot$) of material in the polar regions \cite{Foucart2015}. Over longer timescales, the neutrino-powered winds become active and eject material in the polar regions. Though the material is still negligible compared to the material ejected dynamically in the equatorial plane during the disruption of the neutron star, this ejecta could impact the formation of a relativistic jet \cite{Foucart2015}. Nevertheless, a few percents of the energy radiated in neutrinos is expected to be deposited in the region along the spin axis of the black hole through $\nu\bar{\nu}$ annihilations \cite{Setiawan2006, Janka1999}. The energy deposition at a rate $\sim 10^{51}$ erg s$^{-1}$ might also be able to power short $\gamma$-ray burst \cite{Foucart2014, Lee2007}.

As in the BNS merger scenario, the magnetic mechanism may be more promising in launching ultra-relativistic outflows and then giving rise to GRBs. In the recent high-resolution numerical-relativity simulations for the merger of BH-NS binaries that are subject to tidal disruption and subsequent formation of a massive accretion torus, the accretion torus formed quickly and the magnetic-field was amplified significantly due to the non-axisymmetric magnetorotational instability and magnetic winding \cite{Paschalidis2015, Kiuchi2015}. The amplification can yield $B \sim 10^{15}$ G at the BH poles in ~20 milliseconds after the merger and the
corresponding Blandford-Znajek luminosity can be sufficient high to power GRBs.

For the role of the magnetic process in extracting the energy for the GRBs, the data of GRB 060614 likely has shed valuable light on. Such a long-short event is most likely powered by the merger of a binary system of neutron star and stellar mass black hole (Yang et al. 2015; Jin et al. 2015). As found in various numerical simulations, the total mass of the accretion disk is expected to be not much more massive than ~ 0.1 M⊙. On the other hand, the duration of the “long-lasting” soft γ-ray emission is ~ 100 s. Hence the time averaged accretion rate is expected to be just in order of \( \dot{m} \sim 10^{-3} \) M⊙ s\(^{-1}\). For such a low accretion rate, the neutrino mechanism is expected to be unable to launch energetic GRB outflow (e.g., Fan et al. 2005; Liu et al. 2015). Instead, the Blandford–Znajek process can give rise to Poynting-flux-dominated outflow with an “intrinsic” luminosity \( L_{\text{BZ}} \approx 6 \times 10^{37} \text{ erg s}^{-1} (\alpha/0.75)^2 (B_{\text{BZ}}/10^{-4})^2 \) (Blandford & Znajek 1977), which is sufficient to explain the observed γ-ray luminosity of GRB 060614 after the correction of a jet opening angle of the outflow \( \theta_i \approx 0.1 \) (see Xu et al. 2009). Therefore, the soft long-lasting gamma-ray “tail” emission of GRB 060614 likely has a moderate to high linear polarization (Fan et al. 2005).

In view of these facts, we suggest that ultra-relativistic outflows may be launched within \( \Delta t_{\text{ll RR}} \sim 10 \text{ milliseconds} \) after the BH-NS mergers via either the neutrino-antineutrino annihilation or magnetic process(es).

### 3.2. \( \Delta t_{\text{em}} \) expected in baryonic and magnetic outflow models

#### 3.2.1. The baryonic outflow

The neutrino-antineutrino annihilation process will launch an extremely-hot fireball. For such a kind of baryonic outflow, the acceleration is well understood (Piran et al. 1993; Mészáros et al. 1993) and most of the initial thermal energy may have been converted into the kinetic energy of the baryons at the end of the acceleration (Shemi & Piran 1990). A quasi-thermal emission component, however, is likely inevitable (see Chhotray & Lazatti 2015 and the references therein for the resulting spectrum). The quasi-thermal emission is mainly from the photosphere at a radius \( R_{\text{ph}} \), which can be estimated as \( R_{\text{ph}} \sim 4 \times 10^{10} \text{ cm} \left( L/10^{51} \text{ erg s}^{-1} \right)^{1/3} \left( \eta/200 \right)^{1/2} \left( R_{\odot}/10^{3} \text{ cm} \right)^{1/3} \). And the quasi-thermal radiation peaks at a temperature \( T_{\text{rh}} \sim 80 \text{ keV} \left( L/10^{51} \text{ erg s}^{-1} \right)^{1/4} \left( \eta/200 \right)^{1/2} \left( R_{\odot}/10^{3} \text{ cm} \right)^{1/6} \). For the sources within the advanced LIGO/VIRGO detection ranges (i.e., \( D \approx 300 \text{ Mpc} \)), the energy flux can be high up to \( F \sim 2 \times 10^{-6} \text{ erg s}^{-1} \left( L/10^{51} \text{ erg s}^{-1} \right)^{1/4} \left( \eta/200 \right)^{1/2} \left( R_{\odot}/10^{3} \text{ cm} \right)^{1/6} \), which is detectable for Swift or Fermi-GBM. The acceleration timescale of the baryonic is \( \sim (1+\zeta)R_{\odot}/c \) and the delay between the termination of the acceleration and the emergence of the thermal photons can be estimated as \( \sim (1+\zeta)R_{\odot}/2\eta c \). For \( \eta \geq 100 \) the latter is significantly smaller than the former, hence \( \Delta t_{\text{em}} \sim (1+\zeta)R_{\odot}/c \sim 0.3 \text{ ms} \left( 1+\zeta \right) \left( R_{\odot}/10^{3} \text{ cm} \right) \), which is ignorable small.

If the photospheric quasi-thermal radiation is non-detectable (say, for the NS-BH mergers at \( D \sim 1 \text{ Gpc} \)), more efficient emission may be cased by the collision between the baryonic shells ejected from the same central engine but with much different Lorentz factors. Strong internal shocks are generated and ultra-relativistic particles are accelerated. A fraction of internal shock energy has been converted into magnetic field and the electrons moving in the magnetic field produce energetic γ-ray emission (Rees & Mészáros 1995). In such a model, the variability of the prompt emission likely traces the behavior of the central engine and the onset of the “internal shock emission” is expected to be within the typical variability timescale of the prompt emission that can be \( \sim 1 \sim 10 \text{ ms} \) (Piran 1999), i.e., \( \Delta t_{\text{em}} \sim 1 \sim 10 \text{ ms} \).

#### 3.2.2. The magnetic outflow

In the case of the magnetic outflow, both the acceleration and the subsequent energy-dissipation/radiation are more uncertain (see Kumar & Zhang 2015; Granot et al. 2015 for recent reviews). If the magnetic energy has been effectively converted into the kinetic energy of the outflow (Granot et al. 2015), the prompt emission of GRBs can be from the magnetized internal shocks (Fan et al. 2004) or the photosphere with internal dissipation of energy via gradual magnetic reconnection (Giannios 2008) and we expect \( \Delta t_{\text{em}} \sim 1 \sim 10 \text{ ms} \). Note that in the latest time-dependent 3D relativistic magnetohydrodynamic simulations of relativistic, Poynting-flux dominated jets that propagate into medium with a spherically-symmetric power-law density distribution has found out that some instabilities can leads to efficient dissipation of the toroidal magnetic field component (Bromberg & Tchekhovskoy 2013), for which the onset of the prompt emission is likely dominated by the photospheric radiation and \( \Delta t_{\text{em}} \) is ignorable small.

If the photospheric radiation is too weak to be detectable for Fermi-GBM-like detectors due to either the absence of a dense wind-like medium in the direction of the black hole spin or the small luminosity of the breaking out material, the observed onset of the prompt emission is likely significantly delayed. In some models most of the initial magnetic energy has not been converted into the kinetic/thermal energy of the outflow and the prompt emission of GRBs is due to the magnetic energy dissipation at a rather large distance \( R_{\text{pro}} \sim 10^{16} \text{ cm} \) possibly due to the breakdown of magnetohydrodynamic approximation of the highly-magnetized outflow (Usov 1994; Zhang & Mészáros 2002; Fan et al. 2005), or the current-driven instabilities developed in the outflow shell (Lyutikov & Blandford 2003), or the internal collision-induced magnetic reconnection and turbulence (Zhang & Yan 2013). Correspondingly we have \( \Delta t_{\text{em}} \approx (1+\zeta)R_{\text{pro}}/2\eta^2 c \approx 2 \text{ s} \left( 1+\zeta \right) \left( R_{\text{pro}}/10^{16} \text{ cm} \right) (\eta/300)^{-2} \) (i.e., the radial timescale), which equals to the “angular timescale” of the emission, the minimal timescale of the GRB duration, as long as the ejecta has an opening angle larger than \( 1/\eta \) (Piran 1999). Since the angular timescale is derived for an infinite-thin radiating shell, it is expected to be shorter than the duration of the prompt emission of the whole GRB (i.e., \( \Delta t_{\text{em}} \leq T_{90} \)).

SGR 050509B and SGRB 050709 have \( T_{90} = 0.04 \text{ s} \) and 0.07 s, respectively (Fox et al. 2005). For such “brief” events,

\(^1\) The magnetized internal shocks with significant magnetic dissipation (Fan et al. 2004) can take place at a much smaller radius, say, \( 10^{14} \sim 10^{15} \text{ cm} \).
$R_{\text{pro}} \sim 10^{16}$ cm is disfavored unless $\eta \simeq 2000$. The $\eta$ as high as $\sim 2000$, however, would render them the outstanding outliers of the correlation $\eta \approx 250 \times L_9^{1/5} \text{ erg s}^{-1}^{0.3}$ holding for some long GRBs [Lü et al. 2013; Fan et al. 2012; Liang et al. 2015], and possibly also the short burst GRB 090510 if its $\eta \gtrsim 1200$, as argued in Ackermann et al. (2010), where $L_9$ is the $\gamma$-ray luminosity of the GRB. Moreover, unless there is the fine tuning that the central engine shut down almost at the same time as the outflow breaks out the dense material, the central engines of these two very-short bursts should be (promptly-formed) black holes and $\Delta_{\text{GW-GRB}} < T_{90}$ is expected. For SGRB 050709 the modeling of the macronova signal favors a NS-BH merger origin (Fin et al. 2018), which is in support of our current argument (i.e., the central engine of SGRB 050709 was a black hole).

### 3.3. Expected relationship between $\Delta_{\text{GW-GRB}}$ and $T_{90}$

We summarize in Table 1 the suspected $\Delta_{\text{GW-GRB}}$ (i.e., the sum of $\Delta_{\text{huan}}$ and $\Delta_{\text{em}}$), where the case of $R_{\text{pro}} \ll 10^{16}$ cm includes the scenarios of photospheric radiation and regular (magnetized) internal shock radiation. Clearly, the shortest delay is expected in the cases of prompt BH formation in the NS-NS mergers or the NS-BH mergers if the onset of the prompt emission is governed by the photosphere or regular internal shocks (i.e., $R_{\text{pro}} \ll 10^{16}$ cm) and such events will be valuable in imposing very stringent constraint on the difference between the GW and the speed of light (see Sec. 4 for the details).

In Sec. 3.1.1 we have already mentioned that the prompt formation of BH in BNS mergers is likely uncommon. As long as $R_{\text{pro}} \ll 10^{16}$ cm, one naturally expects that (1) for BNS mergers $\Delta_{\text{GW-GRB}}$ is significantly longer than that of the NS-BH mergers, i.e., $\Delta_{\text{GW-GRB}}(\text{NS-BH}) < \Delta_{\text{GW-GRB}}(\text{BNS})$; (2) for NS-BH mergers, usually $\Delta_{\text{GW-GRB}}$ is expected to be shorter than $T_{90}$, i.e., $\Delta_{\text{GW-GRB}}(\text{NS-BH}) < T_{90}$. While for $R_{\text{pro}} \sim 10^{16}$ cm, we expect that $\Delta_{\text{GW-GRB}}$ should be comparable with $T_{90}$ for both BNS and NS-BH merger powered SGRBs (Note that for some very-shortly lasting events such as SGRB 050509B and SGRB 050709, $R_{\text{pro}} \sim 10^{16}$ cm is most-likely disfavored). Therefore, with reasonable large BNS merger GRB sample and NS-BH merger GRB sample, the statistical distribution of $\Delta_{\text{GW-GRB}}$ and $T_{90}$ for each sample or alternatively the distribution of $\Delta_{\text{GW-GRB}}$ for the combined sample could shed valuable light on the central engine physics.

Are BNS mergers and NS-BH merger events distinguishable in the era of advanced LIGO/VIRGO? It is known that GW observations can efficiently measure the binary’s chirp mass $M \equiv (m_1 m_2)^{3/5}/(m_1 + m_2)^{1/5}$, which however leaves the individual masses undetermined, where $m_1$ and $m_2$ are the gravitational masses of the binary stars, respectively (e.g., Bartos et al. 2013; Hannam et al. 2013). Moreover, the accuracy of the reconstruction of the masses is decreased by the additional mass-ratio-spin degeneracy. Fortunately, in many cases the nature of the binary system can be determined. For instance, considering non-spinning compact objects and a $\rho_s \approx 10$, a $M \gtrsim 2.8 M_0$ implies that one of the binary compact objects has to have a mass $> 3.2 M_0$, above $M_{\text{max}}$ for any reasonable NS models, while a $M \leq 1.2 M_0$ suggest that the mass of both compact objects need to be $< 2 M_0$ unless one of the NSs is smaller than $1 M_0$, in which case the limit to the heavier object is $3 M_0$ (Bartos et al. 2013; Hannam et al. 2013). Together with the expected detection rate of the GRBs with GW signals (see Sec. 4), we think that in the era of the GW astronomy, reasonably large BNS merger GRB samples and NS-BH merger GRBs sample will be available and our goals will be (at least partly) achievable.

### 4. Measuring the Velocity of the Gravitational Wave and Testing the Einstein's Equivalence Principle

#### 4.1. Measuring the GW velocity: the “canonical” approach

According to general relativity, in the limit in which the wavelength of gravitational waves is small compared to the radius of curvature of the background space-time, the waves propagate with the velocity of the light, i.e., $c$ (see Will 1998, and the references). In other theories, the speed $v_g$ could differ from $c$. Let us define the parameter

$$\varsigma \equiv (c - v_g)/c.$$  

If the gravitational wave velocity is subluminal (i.e., $\varsigma > 0$), then cosmic rays lose their energy via gravitational Cherenkov radiation significantly. The detection of ultra-high energy cosmic rays thus imposes a stringent constraint 0 $\leq \varsigma \leq 2 \times 10^{-15}$ (or even $2 	imes 10^{-19}$) (i.e., the “subluminal constraint”), depending on the Galactic or extragalactic origin of such particles (Caves 1980; Moore & Nelson 2001). However, there is no theoretical argument (or pathology) against GWs propagating faster than light (see Nishizawa & Nakamura 2014; Blas et al. 2016, and the references therein) and the weak bounds from radiation damping in binary systems are $\varsigma < -0.01$ (Yagi et al. 2013). The time-lag of arrival times between the GW and the simultaneously radiated photons is

$$\delta t_0 = \frac{1}{c} \int \frac{0}{0} \left(1 + z\right) \left(\frac{c}{v_g} - 1\right) dl = \frac{1}{H_0} \int_0^\infty \left[\frac{\varsigma}{1 - \varsigma}\right] \frac{dr}{\sqrt{\Omega_M (1 + z)^3 + \Omega_L}}$$

where $dl = c dt/[(1 + z) H_0 \sqrt{\Omega_M (1 + z)^3 + \Omega_L}]$ is the differential distance the photons have traveled. Note that in this work we take the flat cosmological model (i.e., $\Omega_M + \Omega_L = 1$), $\Omega_M = 0.315$ and $H_0 \approx 70$ km s$^{-1}$ Mpc$^{-1}$ is the Hubble’s constant (Ade et al. 2014; Riess et al. 2011). In general, $\varsigma$ may be a function of the GW frequency ($f$) and especially when graviton mass is non-zero (i.e., $m_{\phi} > 0$) that gives $\varsigma \approx m_{\phi}^2 c^3/2h_f^2$, where $h$ is the Planck’s constant. For simplicity we assume a constant $\varsigma$ and focus on the GW/electromagnetic counterpart association at redshifts $z \ll 1$. Hence eq. (5) yields (see also Will 1998; Nishizawa & Nakamura 2014)

$$\varsigma \approx 5 \times 10^{-17} \left(\frac{200 \text{ Mpc}}{D}\right) \left(\frac{\delta t_0}{1 \text{ s}}\right).$$

In reality usually the photons and the coalescence are not simultaneous and we have $\delta t_0 = (1 + z) \Delta t_c - \Delta t_{\text{GW-ph}}$, where $\Delta t_{\text{GW-ph}}$ and $\Delta t_c$ are the differences in arrival time and emission time, respectively, of the GW and the photons. In most cases, it is rather hard to get a priori value for $\Delta t_c$. Assuming $\Delta t_c = 0$ (i.e., the GW and the electromagnetic counterparts were emitted simultaneously; see Nishizawa 2016 for a more general discussion), we constrain the absolute amplitude of $\varsigma$ as

$$|\varsigma| < 5 \times 10^{-17} \left(\frac{200 \text{ Mpc}}{D}\right) \left(\frac{\Delta t_{\text{GW-ph}}}{1 \text{ s}}\right).$$
almost half of the sky. The Large Synoptic Survey Telescope (LSST) with a field of view / 2014) after 2022. Since advanced LIGO
performance of Einstein Probe (http://www.ptf.caltech.edu). In one full run in 2019, here we just focus on the detectors that
in eq.(7)). The X-ray flares may appear within tens seconds
process material ejected during the merger; (d) the radio radi-
may (still) work at that time and hence will
Note that in some specific cases \( \Delta_{\mathrm{GW}} - \mathrm{GRB} \) is
\( \sim 10^2 \) s/ \( 10^3 \) s or longer. The challenge of
detecting the “orphan” soft X-ray signal is the lack of X-ray
detector(s) with a wide field of view until the successful per-
formance of Einstein Probe (http://ep.bao.ac.cn; Yuan et al.
2014) after 2022. Since advanced LIGO/VIRGO are expected
in full run in 2019, here we just focus on the detectors that
may (still) work at that time and hence will not discuss the
X-ray signal any longer.
If the ultra-relativistic outflow is “on-beam”, the optical/radio afterglow are relatively long-lasting and the peak of the
forward shock optical emission is expected to be within \( 10^2 - 10^3 \) seconds after the merger, mainly depending on
the initial bulk Lorentz factor of the outflow. The optical after-
glow emission of some on-beam GRBs, but missed by the
gamma-ray detector(s), are expected to be detectable for ZTF
and LSST if the bursts are within the sensitivity distance of
advanced LIGO/VIRGO network (see Fig.2). We do not dis-
We call the above process as the “canonical approach” of measuring the GW velocity directly, in which the graviton and photon are assumed to have the same journey (i.e., the Einstein’s equivalence principle (EEP) is guaranteed). The advantage is that as long as a GW/GRB association is established one can constrain \( c_\gamma\) directly. In Sec.4.2 we outline an approach of measuring the GW velocity with a simultaneous test of EEP.
Some widely discussed electromagnetic counterparts of compact object mergers include (Metzger & Berger 2012).
(a) the (short) gamma-ray bursts and X-ray flares; (b) the afterglow emission of the (off-beam) gamma-ray burst outflows;
(c) the macronova/kilonova emission of the sub-relativistic r-
process material ejected during the merger; (d) the radio radia-
tion of the forward shock driven by the sub-relativistic out-
flow launched during the merger. These scenarios hold for both NS-NS and NS-BH mergers (please note that for systems
with very massive BHs, the NSs would be swallowed entirely and no bright electromagnetic counterparts are expected). To constrain \( c_\gamma\) (see eq.(7)), the time delay between the merger and the “emergence” of the electromagnetic counterpart (i.e., \( \Delta_{\mathrm{GW}} - \mathrm{GRB} \)) is needed.

The intense gamma-ray emission is expected to be within seconds after the merger (see Table 1 for the model-dependent estimate, where \( \Delta_{\mathrm{GW}} - \mathrm{GRB} \) is the same as the \( \Delta_{\mathrm{GW}} - \mathrm{ph} \) needed in eq.(7)). The X-ray flares may appear within tens seconds and sometimes may last \( \sim 10^3 \) s or longer. The challenge of
detecting the “orphan” soft X-ray signal is the lack of X-ray
detector(s) with a wide field of view until the successful per-
formance of Einstein Probe (http://ep.bao.ac.cn; Yuan et al.
2014) after 2022. Since advanced LIGO/VIRGO are expected
in full run in 2019, here we just focus on the detectors that
may (still) work at that time and hence will not discuss the
X-ray signal any longer.
If the ultra-relativistic outflow is “on-beam”, the optical/radio afterglow are relatively long-lasting and the peak of the
forward shock optical emission is expected to be within \( 10^2 - 10^3 \) seconds after the merger, mainly depending on
the initial bulk Lorentz factor of the outflow. The optical after-
glow emission of some on-beam GRBs, but missed by the
gamma-ray detector(s), are expected to be detectable for ZTF
and LSST if the bursts are within the sensitivity distance of
advanced LIGO/VIRGO network (see Fig.2). We do not dis-

### Table 1

| Mergers | Prompt Remnant | \( R_{\mathrm{ph}} \approx 10^{16} \) cm | \( R_{\mathrm{ph}} \approx 10^{16} \) cm |
|---------|----------------|-------------------------------------|-------------------------------------|
| BH      | ~ 10 ms        | ~ 2 s(1 + z)(R_{\mathrm{ph}}/10^{16} \) cm/(\eta/300)^2 | ~ 2 s(1 + z)(R_{\mathrm{ph}}/10^{16} \) cm/(\eta/300)^2 |
| BNS     | DRS\(^2\) HMNS | ~ 100 ms                            | 0.1 s + 2 s(1 + z)(R_{\mathrm{ph}}/10^{16} \) cm/(\eta/300)^2 |
|         | TPS\(^3\) HMNS | ~ 1 s                               | ~ 1 + 2 s(1 + z)(R_{\mathrm{ph}}/10^{16} \) cm/(\eta/300)^2 |
|         | GRB--DiINS\(^4\) | ~ 10 - 100 ms                        | ~ 0.1 s + 2 s(1 + z)(R_{\mathrm{ph}}/10^{16} \) cm/(\eta/300)^2 |
| NS--BH  | BH             | ~ 10 ms                             | ~ 2 s(1 + z)(R_{\mathrm{ph}}/10^{16} \) cm/(\eta/300)^2 |

\(^{a}\) Note that in some specific cases \( \Delta_{\mathrm{GW}} - \mathrm{GRB} \) ~ \( 10^2 - 10^3 \) s are possible (e.g. Charisi et al. 2015; Rezzolla & Kumar 2015), which can be easily distinguished from the scenarios summarized in this table as long as a sample of GW/GRB association has been established.

\(^{b}\) Note that in general \( T_{\mathrm{GRB}} \geq 2 s(1 + z)(R_{\mathrm{ph}}/10^{16} \) cm)/(\eta/300)^2. For SGRs, unless (\( R_{\mathrm{ph}}\)/10^{16} \) cm)/(\eta/300)^2 \( \ll 1 \), \( \Delta_{\mathrm{GW}} - \mathrm{GRB} \) is expected to be comparable with \( T_{\mathrm{GRB}} \).

\(^{c}\) DRS is the abbreviation of “Differential rotation supported” and TPS is the abbreviation of “Thermal pressure supported”.

\(^{d}\) GRB--DiINS represents the case of that differentially-rotating NS directly launches GRB outflow (see the last paragraph of Sec.4.1 for the discussion on such a kind of possibility). This case is different from the first three scenarios in which the GRB ejecta is assumed to be launched when the gravitational collapse takes place.

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2 In 2017 the Zwicky Transient Facility (ZTF) with an instantaneous field of view ~ 470 degrees and an r-band sensitivity ~21th mag will have first light at Palomar Observatory (http://www.ptf.caltech.edu/ztf). In one full night the survey field of view is expected to be ~ 2.4 \( \times 10^4 \) square degrees, almost half of the sky. The Large Synoptic Survey Telescope (LSST) with a 9.6 deg\(^2\) field of view that can image about 10,000 square degrees of sky in three clear nights down to limit of ~ 24th magnitude (Vega system) in r-band are expected to play an important role in detecting the nearby GRB afterglow and even the macronovae (Kocevski et al. 2008).

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days while the infrared emission may peak in one or two weeks (see e.g., Li & Paczynski [1998], Barnes & Kasen [2013], Hotokezaka et al. [2013b] for the theoretical predictions; Please see Jin et al. 2015 for the first observed multi-epoch/band macronova lightcurve). As shown in Jin et al. (2016), macronova emission are likely to have a very-promising detection prospect and can serve as ideal electromagnetic signal of the merger events. The typical discovery timescale is likely ~ 1 – 10 days.

We therefore conclude that if the electromagnetic counterparts are (prompt GRB emission, on-beam forward shock emission, macronova emission),

\[ \Delta t_{\text{GW-ph}} \sim 0.01 - 1 \text{ s}, 0.01 - 1 \text{ day}, 1 - 10 \text{ days}, \]

respectively. The expected constraints on \( \varsigma \) are shown in Fig. 3. Possibly in a few years, \(|\varsigma| < 10^{-18}\) is achievable.

### 4.2. Measuring the GW velocity with a simultaneous test of Einstein’s equivalence principle

In this subsection, we consider a simultaneous constraint on the departure of GW velocity from the speed of light and the possible violation degree of EEP with a set of GW/GRB association data. Within the framework of parameterized post-Newtonian approximation (PPN), deviations from EEP are described by the parameter \( \gamma \), which is 1 in general relativity (Will 2014). In general, the Shapiro time-delay is calculated by \( t_{\text{gra}} = \int_{r_e}^{r_o} U(r(t); t) dr \), where the integration is along the path of the photon emitted form the source at \( r_e \) and received at \( r_o \), and \( U(r(t); t) \) is the gravitational potential (Shapiro 1964). If the PPN parameter \( \gamma \) is variable for different species of neutral particles, two kinds of particles emitted simultaneously from the source would arrive at different times, and the corresponding time-lag is governed by \( \Delta t_{\text{gra}} = \int_{r_e}^{r_o} U(r(t); t) dr \) (Longo 1988, Krauss & Tremaine 1988, Sivaram 1999, Shapiro 1964). In this work we focus on the Shapiro time-delay between photons and GWs caused by the gravitational potential of the Milky Way (see Sivaram (1999) for the brief idea and Wu et al. (2016) for the dedicated investigation). Moreover, we adopt the Keplerian potential, for which the Shapiro time-delay can be well approximated by

\[
\Delta t_{\text{gra}} = \frac{GM_{\text{MW}}}{c^2} \ln \left( \frac{D}{b} \right) 
\approx 1.7 \times 10^7 \text{ s} \Delta \gamma \left( \frac{M_{\text{MW}}}{6 \times 10^{11} M_{\odot}} \right) \ln(D/b) \left( \frac{D}{100 \text{ Mpc}} \right) / 4 \ln 10,
\]

where \( M_{\text{MW}} \approx 6 \times 10^{11} M_{\odot} \) is the mass of Milky Way, \( D \) is the distance of the cosmological transient to the Earth, and \( b \) is the impact parameter of the particle paths relative to the Milky Way center, and we have normalized \( \ln(D/b) \) to the value of 4 ln 10 to address the facts that \( D \sim 100 \text{ Mpc} \) in the advanced LIGO/VIRGO era and \( d \sim 10 \text{ kpc} \).

As in the “canonical approach”, we assume that \( v_p \) is a constant. Then the observed time delay consists of three parts, i.e.,

\[ \Delta t_{\text{GW-ph}} = \Delta t_e - \Delta t_o + \Delta t_{\text{gra}}. \]

where \( \Delta t_o \approx 2 \times 10^{16} \text{ s} \varsigma (D/200 \text{ Mpc}) \). In the specific model of “Dark Matter Emulators” the GWs are expected to arrive earlier than the simultaneously-emitted GRB photons by \( \sim 10^3 \) days (Desai et al. 2008). While in reasonable astrophysical models the GW signal should precede the GRB for a given source. Hence an almost simultaneous arrival of the GW/GRB signals requires a subluminal GW with a \( \varsigma \sim 4 \times 10^{-9} (D/200 \text{ Mpc}) \), which violates the “submillimetric constraint” set by the ultra-high energy cosmic rays (i.e., \( 0 < \varsigma < 2 \times 10^{-15} \)) and in turn rules out the Dark Matter Emulators but favors the dark matter model (see also Kahya & Desai 2016 for the discussion on the possible GW150914/GBM transverse association). If two events of GW/electromagnetic counterpart association are observed (which are marked by subscripts 1 and 2, respectively), we have

\[
\Delta \gamma = 5.5 \times 10^{-7} \left( \frac{M_{\text{MW}}}{6 \times 10^{11} M_{\odot}} \right)^{-1} \frac{D_1 \Delta t'_{\text{GW-ph.1}} - D_1 \Delta t'_{\text{GW-ph.2}}}{D_2 \ln(D_1/b_1) - D_1 \ln(D_2/b_2)}
\]

and

\[
\varsigma = 10^{-16} \text{ Mpc} \left[ \frac{\ln(D_2/b_2) \Delta t'_{\text{GW-ph.1}} - \ln(D_1/b_1) \Delta t'_{\text{GW-ph.2}}}{D_2 \ln(D_1/b_1) - D_1 \ln(D_2/b_2)} \right].
\]

where \( \Delta t'_{\text{GW-ph.1}} \equiv \Delta t_{\text{GW-ph.1}} - \Delta t_e,1 \) and \( \Delta t'_{\text{GW-ph.2}} \equiv \Delta t_{\text{GW-ph.2}} - \Delta t_e,2 \) (Note that the relationship \( \Delta t_{\text{GW-ph}} \geq \Delta t_e \), as expected in general relativity, may be invalid for current model assumption). For a set of GW signals with electromagnetic counterparts, the \( (\Delta t_{\text{GW-ph}}, D, b) \) are available and the main uncertainty on constraining \( \varsigma \) and \( \Delta \gamma \) are the accuracy of estimating \( \Delta t_e \). Here we do not simply take \( \Delta t_e \) as zero and focus on the events of SGRBs or short-long GRBs with associated GW signals, for which \( \Delta t_e \) can be relatively reasonably estimated (see Table 1). In particular, for NS-BH merger GRBs we expect that \( \Delta t_e \leq T_90 \) (unless \( T_90 \) is significantly shorter than \( \Delta t_{\text{lim}} \sim 10 \text{ ms} \) that has not been recorded by Swift yet).

The conservative constraints on \( |\Delta \gamma| \) and \( |\varsigma| \) are

\[
|\Delta \gamma| \leq 5.5 \times 10^{-7} \left( \frac{M_{\text{MW}}}{6 \times 10^{11} M_{\odot}} \right)^{-1} \left( |D_2 \Delta t_{\text{GW-ph.1}}| + |D_2 \Delta t_{e,1} - D_1 \Delta t_{e,2}| \right) \frac{|D_2 \ln(D_1/b_1) - D_1 \ln(D_2/b_2)|}{},
\]
GRB 060614, accompanied with a macronova signal that is and further replace GRB 060614, will be unambiguously tested. We hence sug-
grats, as favored by the macronova signature displayed in
compact object binary merger origin of some long-short
events may be due to NS
and

$$|\Delta t_{\gamma} - \Delta t_{\nu}| = \left| \frac{D_2}{b_2} \right| \frac{\ln(D_1/b_1)}{100 \text{ Mpc}} \ln(\frac{D_1}{b_1}) - \frac{D_1}{b_1}\ln(\frac{D_2}{b_2})|, $$

(13)

respectively, where $R \equiv \ln(D_1/b_1)/\ln(D_2/b_2)$. If in the future data people can identify two or more NS-BH merger GRBs
associated with GW signals, as a conservative estimate we take into account the fact that $|\Delta t_{\gamma} - \Delta t_{\nu}| < \Delta t_{\nu} + \Delta t_{\nu}$ and further replace $\Delta t_{\nu}$ by $T_{90}$. For $D_2 \geq 1.5 D_1$, $b_2 \sim b_1$, $\Delta t_{\gamma} \sim \Delta t_{\nu}$, and $T_{90,1} \approx T_{90,2}$, the above two constraints (on $|\Delta t_{\gamma}$ and $|\Delta t_{\nu}|$) further reduce to

$$|\Delta t_{\gamma}| < 6 \times 10^{-8} \left( \frac{M_{\text{MW}}}{6 \times 10^{11} M_\odot} \right)^{-1} \frac{\Delta t_{\gamma} - \Delta t_{\nu}}{\ln(D_1/b_1)/4 \ln 10} $$

(14)

and

$$|\Delta t_{\gamma}| < 10^{-17} \left( \frac{\Delta t_{\gamma} - \Delta t_{\nu}}{\ln(D_1/b_1)/4 \ln 10} \right) \frac{\ln(D_2/b_2)}{\ln(D_2/b_1)/100 \text{ Mpc}} $$

(15)

Interestingly, such constraints can be as tight as the bounds on $\Delta t_{\gamma}$ or $|\Delta t_{\nu}|$ set by excluding either the EEP test or the departure of $\nu_\beta$ from $c$.

5. DISCUSSION

GRBs are widely believed to be powered by the mergers of compact object binaries. Note that the BH–NS merger rate is generally expected to be ~ 1/10 times that of the NS–NS merger rate \cite{Abadie2010}. Hence most GRBs are expected to be from NS–NS mergers and a small fraction of events may be due to NS–BH mergers. Though in the up-

coming era of advanced LIGO/VIRGO network the prospect of detecting GW-associated GRBs is promising, none of the nearby (i.e., $z < 0.2$) GRBs are found within the sen-
sitivity distance of the upcoming advanced LIGO/VIRGO network $D_{\text{BNS}} \approx 400 \text{ Mpc (9/\rho)}$ for $\rho \approx 9$. Such a non-

identification, though still understandable (see eq. (3)), is somewhat disappointing. Interestingly, we find out that GRB 060505, one supernova-less long event (also known as long-

short GRB), if powered by a NS–NS merger, is likely within the distance of $D_{\text{BNS}}(\rho_\alpha \approx 9)$. The other long-short burst GRB 060614, accompanied with a macronova signal that is plausibly powered by a NS–BH merger, is within the distance of $D_{\text{NS–BH}}(\rho_\alpha \approx 9)$. Therefore in the era of GW astronomy, the compact object binary merger origin of some long-short

GRBs, as favored by the macronova signature displayed in GRB 060614, will be unambiguously tested. We hence sug-

suggest that both GRBs and long-short GRBs are prime targets of the advanced LIGO/VIRGO network and γ–ray detec-
tors with wide field of views are encouraged to monitor the sky continually to get the accurate information of the prompt emission properties.

In the era of the advanced LIGO/VIRGO, reasonably large BNS merger samples and NS-BH merger GRB samples are estab-
lishable (see Sec.2). Motivated by such a fact, we have examined the possible distribution of $\Delta t_{\gamma}$ and the relation between $T_{90}$ and $\Delta t_{\gamma}$ for each sample. As summarized in Tab. 1, in the case of $R_{\text{pro}} \ll 10^{16}$ cm that represents the scenarios of photospheric radiation and regular (magnetized) internal shock radiation, it is expected that (1) for BNS mergers $\Delta t_{\gamma}$ is signif-

icantly longer than that of the NS-BH mergers, i.e., $\Delta t_{\gamma} < \Delta t_{\nu}$; (2) for NS-BH mergers, usually $\Delta t_{\gamma}$ is expected to be shorter than $T_{90}$, i.e., $\Delta t_{\gamma} < \Delta t_{\nu}$; (3) for both BNS and NS-BH merger powered SGRBs. The comparison with future real data will be helpful in revealing the central engine physics. We would like to also point out that in some specific astrophysical or new physics scenarios, the GRB may precede the GRB signal significantly (i.e., $\Delta t_{\gamma} > T_{90}$). If such large time-lags indeed presents in the future data, the statistical study of the distribution of $\Delta t_{\gamma}$ can distinguish between the astrophysical model (for example the model proposed in \cite{Rezzolla2015}) for some NS mergers but not for NS-BH mergers) and the new physics (e.g., the supluminal movement of the GW).

To tightly constrain the difference between the GW velocity and the speed of light, the shorter $\Delta t_{\gamma}$ (or the slower $\Delta t_{\gamma}$) the better (see Sec.4.2). If the electromagnetic counterpart of GW signal is GRB, we have $\Delta t_{\gamma} = \Delta t_{\gamma}$. The shortest $\Delta t_{\gamma}$ is expected for the prompt BH formation in the NS-NS mergers or the NS-BH mergers if the onset of the prompt GRB emission is governed by the photosphere or regular internal shocks (i.e., $\Delta t_{\gamma} > 10^9$ s). If such large time-lags indeed presents in the future data, the statistical study of the distribution of $\Delta t_{\gamma}$ can distinguish between the astrophysical model (for example the model proposed in \cite{Rezzolla2015}) for some NS mergers but not for NS-BH mergers) and the new physics (e.g., the supluminal movement of the GW).

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