HIGH-ENERGY GAMMA RAYS FROM STELLAR ASSOCIATIONS

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ABSTRACT

It is proposed that TeV γ-rays and neutrinos can be produced by cosmic rays (CRs) through hadronic interactions in the innermost parts of the winds of massive O and B stars. Convection prevents low-energy particles from penetrating into the wind, leading to an absence of MeV-GeV counterparts. It is argued that groups of stars located close to the CR acceleration sites in OB stellar associations may be detectable by ground-based Čerenkov telescopes.

Subject headings: gamma rays: observations — gamma rays: theory — stars: early-type

1. INTRODUCTION

Several γ-ray sources are thought to be related to early-type stars and their neighborhoods (e.g., Montmerle 1979; Cassé & Paul 1980; Bykov & Fleishman 1992a, 1992b; Bykov 2001, Romero & Torres 2003). Recently, the first (and only) TeV unidentified source was detected in the Cygnus region (Aharonian et al. 2002), where a nearby EGRET source (3EG J2033+4118) has a likely stellar origin (White & Chen 1992; Chen, White, & Bertsch 1996; Romero, Benaglia, & Torres 1999; Benaglia et al. 2001). Here, we explore whether cosmic-ray (CR) illumination of stellar winds of O and B stars can lead to Galactic TeV γ-ray sources.

2. THE MODEL

O and B stars lose a significant fraction of their mass in stellar winds with terminal velocities \( V_\infty \sim 10^3 \) km s\(^{-1}\). With mass-loss rates as high as \( \dot{M}_\text{w} = 10^{-8} \) to \( 10^{-4} \) \( M_\odot \) yr\(^{-1}\), the density at the base of the wind can reach \( 10^{-12} \) g cm\(^{-3}\) (e.g., Lamers & Cassinelli 1999, p. 8). Such winds are permeated by significant magnetic fields and provide a matter field dense enough as to produce hadronic γ-ray emission when pervaded by relativistic particles. A typical wind configuration (Castor, McCray, & Weaver 1975; Völk & Forman 1982; Lamers & Cassinelli 1999, p. 355) contains an inner region in free expansion (zone 1) and a much larger hot compressed wind (zone 2). These are finally surrounded by a thin layer of dense swept-up gas (zone 3)—the final interface with the interstellar medium (ISM). The innermost region size is fixed by requiring that at the end of the free expansion phase (about 100 yr after the wind turns on), the swept-up material is comparable to the mass in the driven wave from the wind, which happens at a radius \( R_{\text{wind}} = \sqrt{3M_\odot/4\pi p_0 V_\infty^3} \) / \( 2/3 \), where \( p_0 \approx m_p n_0 \) is the ISM mass density, with \( m_p \) the mass of the proton and \( n_0 \) the ISM number density. After hundreds of thousands of years, the wind produces a bubble with a radius of the order of tens of parsecs, with a density lower (except that in zone 1) than in the ISM. In what follows, we consider the hadronic production of γ-rays in zone 1, the innermost and densest region of the wind. The matter there is described through the continuity equation \( \dot{M}_\infty = 4\pi r^2 \rho(r) V(r) \), where \( \rho(r) \) is the density of the wind and \( V(r) = V_\infty (1 - R_\infty/r)^{3/2} \) is its velocity. Here \( V_\infty \) is the terminal wind velocity, and the parameter \( \beta \approx 1 \) for massive stars (Lamers & Cassinelli 1999, p. 8). \( R_\infty \) is given in terms of the wind velocity close to the star, \( V_\infty \sim 10^{-5} V_\odot \) as \( R_\infty = R_* (1 - (V_\infty/V_\odot)^{3/2}) \). Hence, the particle density is \( n(r) = M_\infty (1 - R_\infty/r)^{3/2} (4\pi m_p V_\infty r^2) \).

Not all CRs will enter the base of the wind. Although wind modulation has been studied in detail only for the case of the relatively weak solar wind (e.g., Parker 1958; Jokipii & Parker 1970; Köta & Jokipii 1983; Jokipii, Köta, & Merényi 1993), a first approach to determine whether particles can pervade the wind is to compute the ratio (ε) between the diffusion and convection timescales: \( t_\epsilon = 3r^2/D \) and \( t_\tau = 3r/V(r) \), where \( D \) is the diffusion coefficient and \( r \) is the position in the wind. Only particles for which \( \epsilon < 1 \) will be able to overcome convection and enter the dense wind region to produce γ-rays through p-p interactions. The diffusion coefficient is \( \epsilon \sim \lambda V_\infty / (\lambda + V_\infty) \), where \( \lambda \) is the mean free path for diffusion in the radial direction. As in White (1985) and Völk & Forman (1982), the mean free path for scattering parallel to the magnetic field (B) direction is assumed as \( \lambda_\| \approx 10 r_\|$ = \( 10EeB \), where \( r_\$ \) is the particle gyroradius and \( E \) its energy. In the perpendicular direction \( \lambda_\perp \approx r_\$ \). The mean free path in the radial direction is then given by \( \lambda_\perp = \lambda_\| \sin^2 \theta + \lambda\perp \cos^2 \theta \approx 10 \cos^2 \theta + \sin^2 \theta \), where \( \cos^2 \theta = 1 - (r_\$/rV)^2 \). Here, the geometry of the magnetic field is represented by the magnetic rotator theory (Weber & Davis 1967; White 1985; Lamers & Cassinelli 1999, p. 255) \( B_\perp = B_\parallel (V/V_\odot(1 + rR_\odot)^{-2}) \) and \( B_\parallel = B_\parallel (rR_\odot)^{-2} \). The latter equation defines a minimum energy \( E_{\gamma\infty}^\text{min}(r) \) below which the particles are convected away from the wind (shown in Fig. 1, left). Note that \( E_{\gamma\infty}^\text{min}(r) \) is an increasing function of \( r \), so particles that are not convected away in the outer regions of the wind are able to diffuse up to its base. Then \( E_{\gamma\infty}^\text{min}(r) \) can be effectively approximated by \( E_{\gamma\infty}^\text{min}(r \gg R_\odot) \) in subsequent computations. Only particles with energies higher than a few TeV will interact with nuclei in the inner wind and ultimately generate γ-rays, substantially reducing the flux in the MeV-GeV band.

The opacity to pair production of the γ-rays in the UV stellar photon field can be computed as \( \tau(R_\odot, E_\gamma) = \int_0^{R_\odot} N(E_\gamma) \sigma_{\gamma\gamma}(E_\gamma, E_\gamma) dE_\gamma dr \), where \( E_\gamma \) is the energy of the photons emitted by the star, \( E_\gamma \) is the energy of the γ-ray, \( R_\odot \) is the place where the photon was created within the wind, and \( \sigma_{\gamma\gamma}(E_\gamma, E_\gamma) \) is the cross section for γγ pair production (Cox 1999, p. 214). The stellar photon distribution is that of a blackbody peaking at typical star effective temperatures (\( T_{\text{eff}} \)).

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$N(E_p) = |\pi B(h/E_{\gamma})| R_{\odot}^2 /r^2$, where $h$ is the Planck constant and $B(E_{\gamma}) = [2E_{\gamma}^4/(hc)]/e^{E_{\gamma}/kT_{\text{eff}}} - 1$. Shown in Figure 1 (right) is $\tau(R_{\odot}, R_{\star})$ for different photon creation sites ($R_{\star} \ll R_{\text{wind}}$). Gamma-photonons of TeV and higher energies do not encounter significant opacities in their way out of the wind, unless they are created at its very base, hovering over the star (which is unlikely to happen because $R_{\text{wind}} \gg R_{\star}$ and the proton propagates in a high magnetic field environment).

Although we show the opacity for values of the photon energy as low as 100 GeV, most of the $\gamma$-rays will have higher energies, since only protons with $E_p > E_p^{\text{min}}$ will enter the wind. The grey (light grey) box in the figure shows typical energies of $\gamma$-rays for the case of a surface magnetic field $B_s = 10$ G (100 G). There is a large uncertainty about the typical values for the magnetic field in the surface of O and B stars, but recent measurements favor $B_s \approx 100$ G (e.g., Donati et al. 2001, 2002).

### 3. Gamma-Ray and Neutrino Emission

The differential $\gamma$-ray emissivity from $\pi^0$-decays can be approximated by $q_{\gamma}(E_{\gamma}) = 4\pi\sigma_{\gamma}(E_{\gamma}) (2Z_{\pi^0}^{(e)} / A_{\pi^0})(E_{\gamma} \eta_1 \Omega(E_p - E_p^{\text{max}}))$ at the energies of interest. The parameter $\eta_1$ takes into account the contribution from different nuclei in the wind (for a standard composition $\eta_1 \sim 1.5$; Dermer 1986). $J_{\gamma}(E_{\gamma})$ is the proton flux distribution evaluated at $E_{\gamma} = E_p$ (units of protons per unit time, solid angle, energy band, and area). The cross section $\sigma_{\gamma}(E_{\gamma})$ for $p-p$ interactions at energy $E_p \approx 10$ GeV can be represented above $E_{\gamma} \approx 10$ GeV by $\sigma_{\gamma}(E_{\gamma}) \approx 30(0.95 + 0.06 \log (E_{\gamma}/\text{GeV}))$ mbarn (e.g., Aharonian & Atoyan 1996). $Z_{\pi^0}^{(e)}$ is the so-called spectrum-weighted moment of the inclusive cross section. Its value for different spectral indices $\alpha$ is given, for instance, by Drury, Aharonian, & Völk (1994). Finally, $\Omega(E_p - E_p^{\text{min}})$ is a Heaviside function that takes into account the fact that only CRs with energies higher than $E_p^{\text{min}}(r \gg R_{\star})$ will diffuse into the wind. The spectral $\gamma$-ray intensity (photons per unit time and energy band) is $I_{\gamma}(E_{\gamma}) = [n(r)q_{\gamma}(E_{\gamma})dV]$.

### Table 1

Examples for Hadronic $\gamma$-Ray Luminosities from Typical Stellar Wind Configurations

| Model | $V_{\star}$ (km s$^{-1}$) | $n_0$ (cm$^{-3}$) | $R_{\text{wind}}$ (pc) | $M_{\text{wind}}$ (M$_\odot$) | $L_{\gamma}^{1/2}/K_p$ (ergs s$^{-1}$) | $L_{\gamma}^{1/2}/K_p$ (ergs s$^{-1}$) |
|-------|-----------------|------------------|--------------------------|----------------|-----------------|-----------------|
| a     | 1750            | 10               | 0.07                     | 2 x 10$^{30}$ | 7 x 10$^{30}$   | 3 x 10$^{30}$   |
| b     | 1000            | 1               | 0.24                     | 5 x 10$^{30}$ | 2 x 10$^{31}$   | 8 x 10$^{31}$   |
| c     | 1000            | 0.1             | 0.75                     | 2 x 10$^{30}$ | 7 x 10$^{30}$   | 3 x 10$^{30}$   |
| d     | 1000            | 0.24            | 0.01                     | 5 x 10$^{30}$ | 2 x 10$^{30}$   | 8 x 10$^{30}$   |
| e     | 1000            | 1               | 0.09                     | 4 x 10$^{30}$ | 1 x 10$^{30}$   | 6 x 10$^{30}$   |
| f     | 1000            | 0.31            | 0.00                     | 1 x 10$^{30}$ | 5 x 10$^{30}$   | 2 x 10$^{30}$   |
| g     | 1000            | 0.99            | 0.00                     | 4 x 10$^{30}$ | 1 x 10$^{30}$   | 6 x 10$^{30}$   |
| h     | 1000            | 0.31            | 0.00                     | 1 x 10$^{30}$ | 5 x 10$^{30}$   | 2 x 10$^{30}$   |
| i     | 800             | 0.11            | 0.00                     | 5 x 10$^{30}$ | 2 x 10$^{30}$   | 9 x 10$^{30}$   |
| j     | 1000            | 1               | 0.35                     | 7 x 10$^{30}$ | 3 x 10$^{30}$   | 10$^{30}$       |
| k     | 1000            | 0.11            | 0.00                     | 5 x 10$^{30}$ | 2 x 10$^{30}$   | 9 x 10$^{30}$   |
| l     | 1000            | 3.5             | 0.04                     | 2 x 10$^{30}$ | 7 x 10$^{30}$   | 3 x 10$^{30}$   |

### 4. Source Location and Luminosity

The flux expected at Earth from an isolated star can be computed as $F_{\gamma}(E_{\gamma} > 1\text{ TeV}) = (13.4\pi D^2)^{1/2} \int_{\text{t}} [n(r)q_{\gamma}(E_{\gamma}) \times 4\pi r^2 dr] dE_{\gamma}$. The models in Table 1, at 2 kpc, give fluxes in the range $(1 \times 10^{-20} - 7 \times 10^{-18}) K_p$ photons cm$^{-2}$ s$^{-1}$. Hence, there are models for which a small group of $\sim$10 stars in a region velocity, and the mass-loss rate. Very mild dependencies appear with $\beta$ and $R_{\star}$. Table 1 presents results for the luminosity for typical values of all these parameters. We have fixed $M_* = 10^{-3} M_\odot$ yr$^{-1}$, $\beta = 1$, and $R_{\star} = 12 R_\odot$ in this example. The mass contained in the innermost region of the wind, $M_{\text{wind}}$, is also shown. $L_{\gamma} \sim 10^{23}$ ergs s$^{-1}$ can be obtained as the luminosity produced by one particular star; the total luminosity of a group of stars should add contributions from all illuminated winds. Convolving the previous integral with the probability of escape (obtained through the opacity as $e^{-\tau}$) does not noticeably change these results. Finally, it is possible to factor out the normalization in favor of the CR enhancement in the region where the wind is immersed. The CR energy density is $\rho_{\text{CR}} = \int_{E_{\gamma}} [n(E_{\gamma})dE_{\gamma}] = 9.9 K_p \times 10^7$ ergs cm$^{-3}$, where $s$ is the enhancement factor of the CR energy density with respect to the local value, $\rho_{\text{CR}}$ (energies between 1 GeV and 20 TeV). Then, $K_p \sim (0.2 - 0.3)s$. The $\nu + \nu$ neutrino flux $[F_{\nu}(E_{\nu})]$ will be derived from the observed $\gamma$-ray flux $[F_{\gamma}(E_{\gamma})]$ by imposing energy conservation (see Alvarez-Muñiz & Halzen 2002 for details): $\int E_{\gamma} F_{\gamma}(E_{\gamma}) dE_{\gamma} = C \int E_{\nu} F_{\nu}(E_{\nu}) dE_{\nu}$, where the limits of the integrals are $E_{\gamma}^{\text{min}}$ ($E_{\gamma}^{\text{max}}$), the minimum (maximum) energy of the photons [neutrinos], and the prefactor $C$ is a numerical constant of the order of one. Using the resulting $\nu$-flux, the signal for the detection of $\nu$-events can be approximated as (Anchordoqui et al. 2003) $S = T_{\text{obs}} \int dE_{\nu} A_{\text{eff}} F_{\nu}(E_{\nu}) P_{\nu}(E_{\nu})$, whereas the noise will be given by $N = T_{\text{obs}} \int dE_{\nu} A_{\text{eff}} F_{\nu}(E_{\nu}) P_{\nu}(E_{\nu}) \Delta \Omega_{\nu_{\tau = \tau}}$, where $\Delta \Omega$ is the solid angle of the search bin ($\Delta \Omega_{\nu_{\tau = \tau}} \approx 3 \times 10^{-4}$ sr for the ICECUBE telescope; Karle 2002) and $F_{\nu}(E_{\nu}) \lesssim 0.2 \times 10^{-32}$ GeV$^{-1}$ cm$^{-2}$ s$^{-1}$ sr$^{-1}$ is the $\nu + \nu$ atmospheric $\nu$-flux (Volkova 1980; Lipari 1993). Here, $P_{\nu_{\tau = \tau}}(E_{\nu}) \approx 3.3 \times 10^{-11}$ (E/GeV)$^{-2}$ denotes the probability that a $\nu$ of energy $E_{\nu} \sim 1-10^3$ GeV, on a trajectory through the detector, produces a $\mu$ (Gaisser, Halzen, & Stanev 1995). Here $T_{\text{obs}}$ is the observing time and $A_{\text{eff}}$ the effective area of the detector. Those systems producing a detectable $\gamma$-ray flux above 1 TeV are prime candidates to also be detectable neutrino sources (see below).
with a CR enhancement factor of ~100 might be detectable at the level of \( \sim 10^{-14} \) photons cm\(^{-2}\) s\(^{-1}\).

CRs are expected to be accelerated in OB associations through turbulent motions and collective effects of stellar winds (e.g., Bykov & Fleishman 1992a, 1992b). The main acceleration region for TeV particles would be in the outer boundary of the superbubble produced by the core of the association. If there is a subgroup of stars located at the acceleration region, their winds might be illuminated by the locally accelerated protons, which would have a distribution with a slope close to the canonical value, \( n \sim 2 \). For stars out of the acceleration region, the changes introduced in the proton distribution by the diffusion of the particles (a steepening of its spectrum) would render the mechanism for TeV \( \gamma \)-ray production inefficient. This can be seen from Table 1 through the strong dependency of the predicted TeV luminosity on the spectral slope of the particles.

An important assumption in our model is that the diffusion coefficient is a linear function of the particle energy in the inner wind. This is indeed an assumption also in both Volk & Forman (1982) and White’s (1985) models of the particle diffusion in the strong winds of early-type stars, among other studies. Measurements of the solar wind, however, seem to suggest a harder relation with energy (e.g., \( D \propto E^{-0.4-0.5} \)).

The particle density within the TeV source region has been averaged from a velocity range integrated along the line of sight corresponding to 3700 pc and including the core of the Cygnus association. (4) The TeV source will actually be immersed in the zone 2 of the winds of the several powerful stars therein detected, which should have swept the ISM away and diminished its density. Our models (e.g., model g of Table 1), which in fact take for the stellar parameters an average value from the stars in Table 3 of Butt et al. (2003), show that the illumination of the innermost regions of the winds of ~10 stars with a CR enhancement of ~300 in a medium density of about 0.1 cm\(^{-3}\) may be enough to produce the HEGRA detection. The neutrino flux that results from a hadronic production of the TeV \( \gamma \)-ray source would not produce a significant detection in AMANDA II, which is consistent with the latest reports by the AMANDA collaboration (Ahrens et al. 2003). In ICECUBE, however, the signal-to-noise ratio is ~1.8 for 1 yr of observation (for energies above 1 TeV, an effective area of 1 km\(^2\), before taking into account neutrino oscillations effects). If ICECUBE can reach a 1\(^\circ\) \( \times \) 1\(^\circ\) or finer search bin and a km\(^2\) effective area at TeV energies, a long integrating time could distinguish the hadronic origin of the HEGRA detection.

5. APPLICATION: THE UNIDENTIFIED TeV SOURCE

The High Energy Gamma Ray Astronomy (HEGRA) detection in the vicinity of Cygnus OB2, TeV J2032+4131 (Aharonian et al. 2002), presents an integral flux \( F_{\gamma}(E_{\gamma} > 1 \text{TeV}) = 4.5(\pm1.3) \times 10^{-13} \text{ photons cm}^{-2} \text{ s}^{-1} \) in the range 1 TeV, and a \( \gamma \)-ray spectrum \( F_{\gamma}(E_{\gamma}) = B(E_{\gamma}/\text{TeV})^{-2.3} \text{ photons cm}^{-2} \text{ s}^{-1} \text{ TeV}^{-1} \), where \( B = 4.7(\pm2.1_{\text{stat}} \pm 1.3_{\text{sys}}) \times 10^{-13} \) and \( \Gamma = 1.9(\pm0.3_{\text{stat}} \pm 0.3_{\text{sys}}) \). No counterparts at lower energies are currently identified (Butt et al. 2003; Mukherjee et al. 2003). The source flux was constant in the previous section.

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