Ultrafast optical switching of three-dimensional Si inverse opal photonic band gap crystals

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We present ultrafast optical switching experiments on three-dimensional photonic band gap crystals. Switching the Si inverse opal is achieved by optically exciting free carriers by a two-photon process. We probe reflectivity in the frequency range of second order Bragg diffraction where the photonic band gap is predicted. We find good experimental switching conditions for free-carrier plasma frequencies between 0.3 and 0.7 times the optical frequency: we thus observe a large frequency shift of up to \( \frac{\Delta \omega}{\omega} = 1.5\% \) of all spectral features including the peak that corresponds to the photonic band gap. We deduce a corresponding large refractive index change of \( \frac{\Delta n_{Si}}{n_{Si}} = 2.0\% \), where \( n_{Si} \) is the refractive index of the silicon backbone of the crystal. The induced absorption length is longer than the sample thickness. We observe a fast decay time of 21 ps, which implies that switching could potentially be repeated at GHz rates. Such a high switching rate is relevant to future switching and modulation applications. © 2007 American Institute of Physics.

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I. INTRODUCTION

Currently, many efforts are devoted to an intricate class of three-dimensional (3D) metamaterials known as photonic crystals. Spatially periodic variations of the refractive index commensurate with optical wavelengths cause the photon dispersion relations to organize in bands, analogous to electron bands in solids. Generally, frequency windows known as stop gaps appear in which modes are forbidden for specific wave vectors. Experimentally, stop gaps appear as peaks in reflectivity spectra. The strong dispersion in photonic crystals can be used to control the propagation direction of light. Fundamental interest in 3D photonic crystals is spurred by the possibility of a photonic band gap, a frequency range for which no modes exist at all. Tailoring of the photonic density of states by a photonic crystal allows one to control fundamental atom-radiation interactions in solid-state environments. In this context the hallmark of a photonic band gap is the eagerly awaited inhibition of spontaneous emission due to a vanishing density of states.

Exciting prospects arise when 3D photonic band gap crystals are switched on ultrafast time scales. First of all, switching the directional properties of photonic crystals leads to fast changes in the reflectivity. Ultrafast control of the propagation of light, which was demonstrated in two-dimensional (2D) photonic crystals by Ref. 4 is essential to applications in active photonic integrated circuits. Second, switching would also allow the capture or release of photons from photonic band gap cavities, which is relevant to solid-state slow-light schemes. Third, switching 3D photonic band gap crystals provides dynamic control over the density of states that would allow the switching-on or -off of light sources in the band gap.

An optical switching experiment requires a switching magnitude as large as possible, ultrafast time scales, as low
as possible induced absorption, as well as good spatial homogeneity of the index change.\textsuperscript{6} In our experiment we change the refractive index of the semiconductor backbone of the crystal by optically exciting a free-carrier plasma. The refractive index of the excited crystal is well described by the Drude model,\textsuperscript{8} in which the plasma frequency \( \omega_p \) is proportional to the density of excited carriers. By carefully choosing the amount of excited carriers, and thus the plasma frequency, large changes in refractive index are feasible, while the induced absorption is predicted to remain small.\textsuperscript{6} For Si, good experimental conditions are found for free-carrier plasma frequencies around \( \omega_p = 0.3\ldots0.7 \times \omega_{\text{probe}} \) where \( \omega_{\text{probe}} \) is the frequency of the probe light. The spatial homogeneity of the excited carrier plasma can be optimized by choosing a two-photon excitation mechanism rather than a linear process.\textsuperscript{9} In Si photonic crystals, optimum spatial homogeneity is obtained for pump frequencies near the two-photon absorption edge of Si \( \omega/c = 5000 \text{ cm}^{-1} \) (\( \lambda = 2000 \text{ nm} \)).\textsuperscript{6}

A pioneering study of switching 3D photonic materials was done by Mazurenko \textit{et al.},\textsuperscript{10} who reported reflectivity changes in silica opaline matrices that were infiltrated with Si. This experiment suffered from several limitations; first, the limited refractive index contrast was insufficient for a band gap to open up. Second, since the experiments were performed at probe frequencies above the electronic band gap of Si, the transparency of the unswitched crystal is limited by intrinsic absorption. Moreover, due to a short Drude damping time for amorphous Si \( \tau_{\text{Drude}} = 500 \text{ fs} \), the maximum feasible refractive index change is limited by the amount of induced absorption. Original switching experiments in Si inverse opals were reported by Becker \textit{et al.} who studied transmission changes.\textsuperscript{11} The induced absorption in their crystal was strongly reduced by annealing the Si backbone, causing \( \tau_{\text{Drude}} \) to increase drastically from 0.5 fs to 10 fs, resulting in a strong reduction of the induced absorption. Unfortunately, however, this study was limited to the frequency range of first order Bragg diffraction where a pseudogap is expected, but not the photonic band gap.

In this article we study ultrafast switching of inverse opal photonic band gap crystals. There are several reasons why inverse opals are highly suitable for all-optical switching experiments. First, their fabrication is relatively simple, which has allowed inverse opals to be studied extensively. The abundance of prior static reflectivity experiments helps us to interpret our switching data.\textsuperscript{12-16} Second, the thickness of opaline crystals is not limited by the fabrication process, in contrast to crystals that are grown by lithographic techniques.\textsuperscript{17} Third, band structure calculations for inverse opals are easily available,\textsuperscript{18,19} facilitating the interpretation of the observed stop bands in our spectra. Fourth, the crystals can have a sufficiently large refractive index contrast for a band gap to open up in the range of second order Bragg diffraction,\textsuperscript{20} while in the range of first order Bragg diffraction a pseudogap occurs.\textsuperscript{21} In the region of the band gap, switching is expected to lead to ultrafast changes in the density of states.\textsuperscript{6} Finally, experimental control of the dynamics of spontaneous emission from quantum dots inside static photonic crystals was recently demonstrated with inverse opals.\textsuperscript{3} Thus, it has been predicted that the spontaneous emission of light sources inside such crystals can indeed be switched on and off.\textsuperscript{6} We therefore expect that a study of ultrafast switching inverse opals in the range of second order Bragg diffraction is timely.

\section*{II. EXPERIMENT}

\textbf{A. Sample}

The Si inverse opal photonic crystal was made by infiltrating Si in a silica opaline template. The template was grown on a Si wafer substrate by a vertical controlled drying method.\textsuperscript{22} The resulting 3D silica template extends over 5 \( \times \) 5 mm, and was infiltrated with Si using chemical vapor deposition at 500 °C.\textsuperscript{15} Subsequently, the sample was annealed for one hour at 750 °C in vacuum. During the annealing process, the amorphous Si in the structure crystallizes into poly-Si, as was confirmed by Raman scattering measurements on a separately deposited thin layer of polycrystalline Si that served as a reference sample.\textsuperscript{23,24} Finally, the SiO\textsubscript{2} template was etched away by a buffered hydrofluoric solution, resulting in a high-quality 3D air-sphere crystal that is supported by a poly-Si backbone.

We have obtained the microscopic structure of our on-chip Si inverse opal crystal from high resolution scanning electron micrographs (SEM). From planar and cross-sectional SEM images we infer that our inverse opal is a fcc crystal. The size of the lattice parameter of the fcc-lattice is obtained from Fig. 1, which shows a top view of a \{111\} plane in the crystal. We find the lattice parameter to be \( a = 1427\pm20 \text{ nm} \), by measuring the lattice parameter along the three \{h00\} in-plane lattice directions, which allows us to correct for a 22° tilt of the sample.\textsuperscript{25} From the lattice parameter and the number of terrace steps, we deduce a sample thickness of \( 7 \times d_{111} = 7 \times a/\sqrt{3} = 5.8 \text{ \mu m} \).

We also observe from Fig. 1 that the interstices (indicated by arrows) in the \{111\} surface appear to be small. To describe the crystal with band structure calculations, we use a model of close packed air spheres (radius \( r_{\text{in}} = a/\sqrt{8} \)) surrounded by spherical shells (radius \( r_{\text{out}} \)) connected by cylindrical windows (radius \( r_{\text{cyll}} \)). From the almost filled interstices in Fig. 1, we estimate an outer shell radius of \( r_{\text{out}} = 1.15\pm0.02 r_{\text{in}} \). The radius of the air holes that inter-
Our setup consists of a regeneratively amplified Ti:Sapphire laser (Spectra Physics Hurricane) which drives two optical parametric amplifiers (OPA, Topas). Both OPAs have a continuously tunable output frequency between 3850 and 21050 cm\(^{-1}\), with pulse durations of 150 fs and a pulse energy \(E_{\text{pulse}}\) of at least 20 \(\mu\)J. The independent tunability of our OPAs allows us to optimize the pump frequency, while scanning the probe frequency over a broad frequency range. The pump beam is incident at \(\theta=15^\circ\), and has a much larger Gaussian focus of 133 \(\mu\)m full width at half maximum (FWHM) than the probe, providing good lateral spatial homogeneity. The probe beam is incident at normal incidence \(\theta=0^\circ\), and is focused to a Gaussian spot of 28 \(\mu\)m FWHM at a small angular divergence \(N\Delta=0.02\). Therefore, we ensure that only the central flat part of the pump focus is probed. The reflectivity was calibrated by referencing to a gold mirror. A versatile measurement scheme was developed to subtract the pump background from the probe signal, and to compensate for possible pulse-to-pulse variations in the output of our laser, see Ref. 17.

III. RESULTS AND DISCUSSION

A. Linear reflectivity spectra

The linear reflectivity spectra in Fig. 2(b) demonstrates three stop bands in the frequency range \(\omega=5000–7000\text{ cm}^{-1}\), similar to earlier work.\(^{13–16}\) We compare them to a calculated band structure diagram, and label the stop bands. Stop band I at frequency \(\omega=5320\text{ cm}^{-1}\) displays a maximum reflectivity \(R=51\%\) and is identified with the \(\Gamma-L\) stop gap at frequency \(a/\lambda=0.76\) in the calculated band structure shown in Fig. 2(a). At \(\omega=5950\text{ cm}^{-1}\), we observe a stop band, labeled II, with maximum reflectivity \(R=60\%\). Stop band II corresponds to the stop gap at \(a/\lambda=0.85\) in Fig. 2(a). It is important to note that stop band II overlaps the frequency range of the predicted band gap that is centered around \(a/\lambda=0.85\). Stop band III at \(\omega=6500\text{ cm}^{-1}\) aligns with the stop gap at \(a/\lambda=0.94\). The frequency of the small peak at \(\omega=7616\text{ cm}^{-1}\) matches that of the stop band at \(a/\lambda=1.08\).

We have systematically reproduced our data on various positions on the sample. The peak reflectivity of all peaks varies by less than 10\% with position. The variation is possibly due to variations in the density of lattice defects throughout the crystal. The center frequency of the stop bands, however, were found to be independent of position on the sample (within \(\Delta\omega/\omega<1\%\)), which leads to the important conclusion that the crystal lattice is indeed the same everywhere in the sample.

The agreement between reflectivity peaks and theoretical stop gaps demonstrates that expected surface effects do not impede the ability of exploiting reflectivity measurements to probe bulk properties. We must note that, despite the apparent good agreement, a direct comparison between reflectivity data and band structure calculations is strictly speaking not allowed, since band structure calculations assume an infinitely extended crystal, and do not take into account surface effects. For instance, a large impedance mismatch of external modes and internal modes as a result of flat bands in the band structure can also lead to an increased reflectivity. A stop gap in the band structure calculations, however, should always result in an increased reflectivity, which is indeed the case here.

B. Switched reflectivity spectra

We have induced large and ultrafast reflectivity changes in our crystal by optically exciting free-carriers. The ultrafast
response of the stop bands is acquired by measuring the reflectivity spectra at fixed probe delays. In experiments on the red part of the spectrum ($\omega_{\text{probe}} < 6250 \text{ cm}^{-1}$), the pump frequency was chosen to be $\omega_{\text{pump}} = 6450 \text{ cm}^{-1}$. In experiments on the blue edge ($6250 \text{ cm}^{-1} < \omega_{\text{probe}}$), the pump frequency was reduced to $\omega_{\text{pump}} = 5000 \text{ cm}^{-1}$. The switched reflectivity spectra were measured in the same run and on the same spot on the sample as the linear data are shown as closed circles in Fig. 2(b). Due to dispersion in the probe path of the setup, there is a <500 fs variation of the delay time with frequency, we therefore measure the switched reflectivity at a fixed time delay of $\tau = 1$ ps. Figure 2(b) shows measurements of the switched and linear reflectivity in the range of second order Bragg diffraction of the sample at normal incidence.

The dispersion and propagation of light in the crystal is strongly modified by the switching. Consequently, we observe large variations in the reflectivity near the peaks in the region of second order Bragg diffraction. On the red edge of peak I, near $\omega = 5110 \text{ cm}^{-1}$, the reflectivity strongly decreases, while on the blue edge, at $\omega = 5500 \text{ cm}^{-1}$, we observe a strong increase in the reflectivity, indicative of a blueshift of the entire peak. Our crystals are therefore highly suitable to control the directional propagation of light.

The magnitude of the frequency shift of the peaks was obtained by measuring the frequency position of the red edge of stop band I, indicated by the black arrow in Fig. 2(b). The switching moves the edge toward higher frequencies, while the slope of the stop band edge remains unchanged. Only at the highest intensity used, induced absorption can slightly change the slope of the edge. However, the contribution of this effect to the measured shift is negligibly small.

The blueshift of peak I is as large as 80 cm$^{-1}$ or $\Delta \omega / \omega = 1.5\%$. The same effect occurs on the red edge of peak II, near $\omega = 5800 \text{ cm}^{-1}$, where the reflectivity decreases, and on the blue edge of peak III, near $\omega = 7000 \text{ cm}^{-1}$, where the reflectivity increases. The blue edge of stop band III has blueshifted by 50 cm$^{-1}$ or $\Delta \omega / \omega = 0.7\%$. Importantly, all stop bands have shifted toward higher frequency. We therefore conclude that switching has reduced the average refractive index of the crystal.

The shift of the stop bands is clearly evidenced by the dispersive features in the differential reflectivity of the sample that is plotted in Fig. 2(c). On the red edge of stop band I, at $\omega = 5110 \text{ cm}^{-1}$, we observe a large decrease in the reflectivity by $\Delta R / R = 54\%$, while at $\omega = 5500 \text{ cm}^{-1}$ we observe a strong increase in the reflectivity by $\Delta R / R = 49\%$. This distinct dispersive shape that is centered at around 5320 cm$^{-1}$ is related to a large blueshift of the combined stop bands II and III. The strong dispersive curve that is centered around $\omega = 7600 \text{ cm}^{-1}$ shows that the small peak at this frequency also shifts toward higher frequency.

The observed shift of stop band II toward higher frequency is particularly interesting, as this stop band is part of the predicted band gap for inverse opals. We have thus demonstrated switching of a 3D photonic band gap, which has not been reported before. The switching process is expected to lead to ultrafast changes of the density of states inside the crystal.

Remarkably, we observe that both the low and high frequency edge of the stop bands have shifted. This indicates the absence of separate dielectric and air bands in the range of second order Bragg diffraction in inverse opals, which is consistent with predictions based on quasistatic band structure calculations by Ref. 6. From our comparison we find a refractive index change of $\Delta n / n = 2\%$ and a carrier density of $N_p = 2.1 \times 10^{19} \text{ cm}^{-3}$. The corresponding plasma frequency is $\omega_p = 3623 \text{ cm}^{-1}$, which is equal to $0.72 \times \omega_{\text{probe}}$. We conclude that excellent switching conditions indeed appear if the plasma frequency $\omega_p$ remains smaller than the probe frequency as predicted in Sec. I.

C. Switching time traces

The large and ultrafast shift of the stop band with time is studied in detail in Fig. 3. We have measured the frequency position of the red edge of the stop band at $\omega = 5045 \text{ cm}^{-1}$, at a large range of delay times after excitation. From each spectrum, the frequency position of the low frequency edge was determined at $R = 15\%$ [indicated by the arrow in Fig. 2(b)]. The relative frequency shift $\Delta \omega / \omega$ is plotted versus probe delay in Fig. 3. We observe a large and ultrafast shift of the stop band edge from 0 to $\Delta \omega / \omega = 1.1\%$ with an exponential growth time of $\tau = 500$ fs, limited by the pulse duration of our pump pulses.

The effect subsequently decreases exponentially with a decay time of $\tau = 21 \pm 4$ ps (least-squares fit) to a small residual shift $\Delta \omega / \omega = 0.1\%$. The decay times are much faster related to a large blueshift of the combined stop bands II and III. The strong dispersive curve that is centered around $\omega$ = 7600 cm$^{-1}$ shows that the small peak at this frequency also shifts toward higher frequency.
Since only a fraction of the light is transmitted in Sec. II A, to describe our crystal as an effective medium consisting of Si and air. In more advanced studies, the reflectivity peak, which is associated with an increase in the reflectivity maximum after excitation. We therefore plot the relative decrease in reflectivity maximum of woodpile samples to the induced absorptivity range. The induced absorption manifests itself in a reduction of the reflectivity of the whole sample, while it should not affect the frequency positions of the stop bands in Fig. 2, which are related to changes in the backbone of the photonic crystal only. Indeed, we find that the stop band shift in Fig. 3 decays rapidly within 100 ps, to a small offset of a few wave numbers. Meanwhile, a large part of the reflectivity decrease in Fig. 4 is still present after 100 ps and continues to decay on ns time scales, consistent with the slow recombination of carriers in the wafer substrate.

In our experiments we have used two-photon absorption at long pump wavelengths combined with a large pump focus to maximize the spatial homogeneity of the switched crystals. The pump fluence in our experiments was typically 25 pJ per unit cell area per pulse. In applications with small active areas, typical for 2D and 3D cavities, spatial homogeneity is not an important issue and thus low pump fluences suffice. Furthermore, the pump fluence can be further reduced by choosing the pump wavelength in the linear absorption range.

V. CONCLUSIONS

In this article, we have studied all-optical ultrafast switching of a high-quality 3D Si inverse opal photonic band gap crystal in the frequency range of second order Bragg diffraction. A spatially homogeneous free-carrier plasma was optically excited in the crystal by a two-photon process. We show that for Si inverse opals, good experimental conditions are found for free-carrier plasma frequencies around \( \omega_p = 0.3 - 0.7 \times \omega_{probe} \); large changes in the refractive index can be achieved, while the crystal remains transparent after the switching. We find good agreement between the stop bands in the linear reflectivity spectra and calculated stop gaps in the frequency range of the band gap. Switching effects are studied as a function of time delay between pump and probe pulses. Large ultrafast variations in reflectivity are observed in the range of second order Bragg diffraction. During the decay times. The fast relaxation process is likely related to the fast recombination of carriers in the poly-Si backbone of the crystal that was discussed in the previous section. It is presently unclear why the induced absorption decays about five times faster than the induced stop band shift shown in Fig. 2(b), which was obtained from the same set of spectra. The subsequent, much slower recombination process at ns times is attributed to recombination of excited carriers in the underlaying Si-wafer substrate. In bulk Si at the carrier densities in our experiment (10^19 cm^-3), carrier recombination is dominated by Auger effects with recombination times of the order of 10 ns. Any change in the substrate is likely to change the magnitude of the reflectivity of the whole sample, while it should not affect the frequency positions of the stop bands in Fig. 2, which are related to changes in the backbone of the photonic crystal only. Indeed, we find that the stop band shift in Fig. 3 decays rapidly within 100 ps, to a small offset of a few wave numbers. Meanwhile, a large part of the reflectivity decrease in Fig. 4 is still present after 100 ps and continues to decay on ns time scales, consistent with the slow recombination of carriers in the wafer substrate.

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switching process, all spectral features in the observed stop bands, shift toward higher frequencies by as much as $\Delta \omega / \omega = 1.5\%$ within a few hundred fs, indicating the absence of separate dielectric and air bands in our crystal. From a comparison to quasistatic band structure calculations of Ref. 6 we infer a large refractive index change of about 2. We have observed a relatively fast decay time of 21 ps, which implies that switching could potentially be repeated at a GHz rates, which is relevant to possible future switching and modulation applications.

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