Diagrammatic Cancellations and the Gauge Dependence of QED

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Abstract

This letter examines diagrammatic cancellations for Quantum Electrodynamics (QED) in the general linear gauge. These cancellations combine Feynman graphs of various topologies and provide a method to reconstruct the gauge dependence of the electron propagator from the result of a particular gauge by means of a linear Dyson-Schwinger equation. We use this method in combination with dimensional regularization to demonstrate how the 3-loop $\varepsilon$-expansion in the Feynman gauge determines the $\varepsilon$-expansions for all gauge parameter dependent terms to 4 loops.

Keywords: cancellation, Dyson-Schwinger equation, Feynman graph, gauge dependence, quantum electrodynamics, renormalization

1. Introduction

Our ability to perform high-order calculations in perturbative Quantum Field Theory is limited due to the enormous number of Feynman graphs which need to be evaluated. A graph-by-graph evaluation fails to exploit global symmetry properties, such as the Ward or Slavnov-Taylor identities, which are only satisfied by the sum of a certain subclass of Feynman graphs. However, for abelian as well as non-abelian gauge theories, it is well understood that these global identities originate from the pure structure of propagator and vertex Feynman rules and their resulting cancellations between certain tree-level Feynman graphs \cite{1, 2, 3, 4, 5, 6}. Although these combinatorial arguments are considered to be rather inconvenient and lengthy in comparison to a BRST derivation, there are at least three potential benefits for exploiting these cancellations in perturbative Quantum Field Theory.

- The perturbative expansion given in terms of Feynman graphs might be rearranged in terms of meta graphs or subsectors with a maximum number of cancellations implemented. For example, an early attempt to construct gauge invariant subsectors in QCD was given by Cvitanović et al. \cite{7}.

- An explicit implementation of a cancellation identity into computational procedures reduces the number of terms which need to be evaluated, for example Herzog et al. pointed out that contracting all legs of a three-gluon vertex with the corresponding momenta yields a vanishing contribution \cite{8, 9}. Similar more general identities on gauge theory amplitudes lead to the graph and cycle homologies observed in \cite{5}.

- Cancellation identities provide all-order restrictions for the structure of Green’s function, for instance certain tree-level identities guarantee the transversality of the photon or gluon self-energy. This can be exploited to simplify calculations or provide a non-trivial check.

This letter provides an insight into how the QED tree-level identity implies cancellation between Feynman graphs of different topologies and determines the gauge dependence.

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2. The QED cancellation identity

This section discusses the QED cancellation identity and its implications. Special emphasis is given to the electron propagator.

Consider the Lagrangian of Quantum Electrodynamics in the linear covariant gauge with fermions of mass $m$

$$L_{\text{QED}} = -\frac{1}{4} F_{\mu\nu} F^{\mu\nu} + \frac{1}{2} (\partial_\mu A^\mu)^2 + \bar{\psi}(i\slashed{D} - m) \psi.$$  \hfill (1)

This parametrization of the gauge parameter $\xi$ is especially convenient for perturbative calculations as it minimizes the number of terms in the photon propagator

$$P^{\mu\nu}(k) = -i \frac{g^{\mu\nu}}{k^2} - \xi \frac{k^\mu k^\nu}{(k^2)^2}.$$  \hfill (2)

A generic Feynman graph evaluates to a polynomial in $\xi$. The constant term of this polynomial is derived by setting all photon propagators in the Feynman gauge ($\xi = 0$). Terms of higher powers in $\xi$ can be constructed by replacements of these Feynman-gauged propagators by the gauge dependent term of the photon propagator. For instance, the term linear in $\xi$ corresponds to the summation over all possibilities to replace one of the photon propagators which are in the Feynman gauge by a gauge dependent Lorentz tensor

$$-k_\mu \frac{1}{k^2} (-i\xi) \frac{1}{k^2} k^\nu.$$  \hfill (3)

In a Feynman graph, this tensor connects two electron-photon vertices and both of these vertices are contracted with their ingoing photon momentum. The result of such a contraction is the content of the famous tree-level identity \cite{10}

\begin{equation}
\begin{aligned}
\frac{1}{\slashed{p} + \slashed{k} - m} \gamma_\nu k^\nu & \frac{1}{\slashed{p} - m} = \\
\frac{1}{\slashed{p} - m} - \frac{1}{\slashed{p} + \slashed{k} - m},
\end{aligned}
\end{equation}

(4)

The second line introduces some graphical notation: the contraction of the vertex with its ingoing photon momentum is represented by attaching a triangle on top of the wavy photon line, cancelled fermion propagators are visualized by slashed fermion lines, the remaining dashed line inserts the photon momentum at the vertex, but without contributing the usual $\gamma^\nu$ vertex factor.

The successive iteration of this tree-level identity implies the QED cancellation identity

\begin{equation}
\begin{aligned}
\cdots + \cdots + \cdots = \cdots - \cdots - \cdots.
\end{aligned}
\end{equation}

(5)

It should be remarked that there is no restriction on the photon lines below the horizontal fermion line — pairs of them might be connected with propagators in the Feynman gauge, the gauge dependent Lorentz tensor \cite{9}, or vacuum polarization graphs. This feature enables the tree-level identity to describe cancellations between Feynman graphs at a particular loop order.

As a result, these tree-level identities guarantee the Ward-Takahashi identity.

For instance, the transversality of the vacuum polarization follows from equation (5) by closing the horizontal electron line to a fermion loop and using the momentum routing invariance such that the right-hand side of the equation vanishes. The second consequence of an iterative application of suchlike cancellations implies that the summation over all insertion places of the tensor \cite{9} into all vacuum polarization graphs yields a vanishing contribution, i.e. the vacuum polarization is independent of the gauge parameter.
Further, it is possible to give a diagrammatic derivation \([1, 11]\) of the identity
\[ k^\mu \Lambda_{\mu}(k, p) = \Sigma(p) - \Sigma(p + k) \] (6)
which relates the amputated vertex function \(\Lambda_{\mu}\) to the self-energy of the electron \(\Sigma\). Therefore, we might concentrate our discussion on the latter.

Indeed, all gauge dependent Feynman graphs of the connected electron propagator function \(S\) can be constructed from this cancellation identity. In order to derive the term linear in the gauge parameter \(\xi\) it is necessary to sum over all possible insertions of the gauge dependent tensor \([3]\). This corresponds to attaching a second momentum-contracted photon leg on the horizontal fermion line in the cancellation identity \([5]\). After summation over all possible insertion places, the cancellation identity can be iteratively used to reduce all momentum-contracted photon lines to dashed lines, which are attached to the ends of the horizontal fermion line.

An application of this procedure produces the following cancellation between Feynman graphs at two loops and linear in \(\xi\).

Here, the scalar part of the gauge dependent tensor \([3]\) is represented by the dashed propagator lines which enclose a dot to denote the \(\xi\) factor. As seen by the first graph, the summation over all insertion places requires us to consider connected rather then one-particle irreducible Feynman graphs. The two tadpole graphs are weighted by a combinatorial factors of \(1/2\), which originates from the fact that the summation over all insertion places overcounts graphs which are symmetric under interchange of the momentum-contracted photon legs. Remarkably, this two-loop example demonstrates how Feynman graphs of the T1, T2, and T3 Mincer topologies \([12]\) combine and beside the vanishing tadpoles, only a T2 topology graph remains. Eventually, the two-loop gauge dependent term is constructed by inserting the one-loop propagator into a one-loop skeleton graph.

This observation generalizes to the full connected electron propagator by means of a linear Dyson-Schwinger equation. The electron propagator is expanded into coefficients \(c_{n, l}\) of loop order \(n\) and order \(l\) in the gauge parameter
\[ S(q, m) = \frac{i}{q - m} + \sum_{1 \leq n \leq l \leq n} c_{n, l} \xi^l \alpha^n. \] (8)

These coefficients depend on the momentum \(q\) and the mass \(m\), \(c_{n+1, l+1}(q, m)\), and can be constructed by attaching \((l + 1)\) pairs of momentum-contracted photon legs on the horizontal fermion line and connecting the remaining photon legs by the Feynman-gauged propagator or vacuum polarization graphs in all possible ways. The summation over all possible insertion places of the momentum-contracted photon legs allows for the iterated application of the cancellation identity \([5]\) and implies the linear Dyson-Schwinger equation
\[ c_{n+1, l+1}(q, m) = -\frac{1}{l + 1} e^2 \xi \int \frac{d^4k}{(2\pi)^4} \frac{-i}{[-k^2]^2} c_{n, l}(q + k, m) = -\frac{1}{l + 1} c_{n, l}. \] (9)

This reduction can be iterated and is valid at an arbitrary loop order. The factor \(1/(l+1)\) compensates the overcounting generated by the summation over all insertion places or, in other words, it adjusts for the fact that each of the \((l + 1)\) gauge dependent propagators contribute one term to the cancellation.
3. Gauge-dependent terms to 4 loops

This section focuses on the massless limit of Quantum Electrodynamics. In this limit, the bare electron propagator is analysed by means of the Dyson-Schwinger equation \([20]\) and compared to results obtained by perturbative computations using dimensional regularization.

The skeleton graph of the Dyson-Schwinger equation can be written in terms of the dimensional regularized one-loop master integral of two scalar propagators with weights \(d, \varepsilon, n\)

\[
G(x, y) = -i \int \frac{d^Dk}{(2\pi)^D} \frac{(-q^2 x^2 y^2 - D/2)}{[-k^2]^{1/2} - (k + q)^2} = \frac{\Gamma(D/2 - x)\Gamma(D/2 - y)\Gamma(x + y - D/2)}{(4\pi)^{D/2}\Gamma(x)\Gamma(y)\Gamma(D - x - y)}
\]

(10), where we have amputated the dependence on the external momentum for notational convenience. Recall that the momentum dependence of the \(n\)-loop bare electron propagator \(c_{n,l}(q)\) is given by \(q/(q^2 + l\varepsilon)^n\).

Insertion of this momentum dependence into the Dyson-Schwinger equation determines the contribution of the skeleton graph to the electron propagator. In \(D = d - 2\varepsilon\) dimensions, it contributes the factor

\[
F(d, \varepsilon, n) = \frac{1}{2} \frac{(1 - q^2)^{-\varepsilon}}{(1 + q^2)} [G(\varepsilon/2 - 1, 1 + n\varepsilon) - G(\varepsilon/2, 1 + n\varepsilon) - G(\varepsilon/2, n\varepsilon)] \exp \left[ \varepsilon \left( \frac{\gamma_E + \frac{\zeta(2)\varepsilon}{2}}{2} \right) \right]
\]

(11). Here, \(e\) denotes the bare coupling parameter, \(q\) the external momentum of the electron line, \(\gamma_E\) the Euler–Mascheroni constant and \(\zeta(z)\) is the Riemann zeta function. The exponential factor does not originate from the Dyson-Schwinger equation, but is implemented for straightforward comparison with MINCER results. So far, we are only concerned with the four dimensional case \((d = 4)\) and hence define \(F(\varepsilon, n) := F(4, \varepsilon, n)\) and set \(c_{0,0} := \frac{1}{4}\). Now, an iterative use of the Dyson-Schwinger equation determines all coefficients

\[
c_{n,l} = \frac{1}{l!} c_{n-1,0} \prod_{1 \leq j \leq l} F(\varepsilon, n - j) \text{ for } l \geq 1,
\]

(12) in terms of the Feynman gauge result \(c_{n,0}\) and the one-loop skeleton function \(F\). For instance, the \(\varepsilon\)-expansions of all gauge dependent terms at 4 loops

\[
c_{4,1}(\varepsilon) = c_{3,0}(\varepsilon) F(\varepsilon, 3),
\]

(13) \(c_{4,2}(\varepsilon) = \frac{1}{2!} c_{2,0}(\varepsilon) F(\varepsilon, 3) F(\varepsilon, 2),\)

(14) \(c_{4,3}(\varepsilon) = \frac{1}{3!} c_{1,0}(\varepsilon) F(\varepsilon, 3) F(\varepsilon, 2) F(\varepsilon, 1),\)

(15) \(c_{4,4}(\varepsilon) = \frac{1}{4!} c_{0,0}(\varepsilon) F(\varepsilon, 3) F(\varepsilon, 2) F(\varepsilon, 1) F(\varepsilon, 0)\)

(16) are determined once the \(\varepsilon\)-expansion is known in Feynman gauge at 3 loops. For analytic results of the electron propagator to three loops the reader is referred to \([21, 22, 23, 24]\).

Recall that these coefficients refer to the connected electron propagator \(\mathfrak{S}\). However, for the sake of computational convenience, it is necessary to relate these coefficients to the one-particle irreducible self-energy of the electron \(\Sigma\). Define coefficients \(p_{n,l}\) to decompose the self-energy

\[
\Sigma(q) = q \sum_{1 \leq n} \sum_{0 \leq l \leq n} p_{n,l} \xi^l \alpha^n.
\]

(17)
Then, the relation between the connected and the one-particle irreducible propagator

\[ S(q) = \frac{i}{q - \Sigma(q)} \]  \hspace{1cm} (18)

implies the conversion formulas for the coefficients

\[ \tilde{c}_{n,l} := -i g c_{n,l} = \sum_{k \geq 1} \sum_{n_1 + \cdots + n_k = n} \sum_{l_1 + \cdots + l_k = l} p_{n_1;l_1} \cdots p_{n_k;l_k}, \]  \hspace{1cm} (19)

\[ p_{n,l} = \sum_{k \geq 1} (-1)^{k+1} \sum_{n_1 + \cdots + n_k = n} \sum_{l_1 + \cdots + l_k = l} \tilde{c}_{n_1;l_1} \cdots \tilde{c}_{n_k;l_k}. \]  \hspace{1cm} (20)

In this way, we are able to compare the formula for the coefficient with results from actual perturbative computations. We generate the Feynman graphs of the electron self-energy \( \Sigma \) with QGRAF [25] and perform the computations in FORM [26] and its parallel version TFORM [27] in combination with the MINCER package [28, 12]. From these results, we extract the coefficients \( p_{n,m} \) as a series in \( \varepsilon \) to three loops \( n \leq 3 \) with an arbitrary power in the gauge parameter \( 0 \leq l \leq n \). After the conversion into the connected coefficient (19), the MINCER expansions exactly match the formula (12) derived by means of the linear Dyson-Schwinger equation.

4. Conclusions and outlook

In this letter, we utilized tree-level identities to examine diagrammatic cancellations in QED. In general, these cancellations involve planar as well as non-planar Feynman graphs. Our method applies to an arbitrary order in perturbation theory and allowed us to construct the gauge dependence of the electron propagator to 4 loops from its value in the Feynman gauge. Similar reconstructions are possible if the electron propagator is known in a different linear covariant gauge — we explicitly checked this for the Landau gauge.

Remarkably, the result of a specific gauge at particular loop order determines all gauge terms even at the next loop order and the recursion (12) provides a closed-form expression of the coefficients proportional to \( \alpha^n \xi^n \) at an arbitrary loop order \( n \).

These results follow from the linear Dyson-Schwinger equation (9), which might be of interest for non-perturbative studies. However, the dipole scalar propagator introduces an infrared singularity in the kernel of the skeleton. In contrast to usual ultraviolet divergences, this infrared singularity is not regularized by insertion of an ansatz for the renormalized electron propagator into the Dyson-Schwinger equation. A suitable method to construct a renormalized Dyson-Schwinger equation might be the implementation of cancellation identities into the Hopf algebra of QED [29, 30].

Recently, gauge theories in higher dimensions attracted great interest, because of the interconnection of infrared and ultraviolet fixed points of various dimensions [31, 32]. At \( d = 4, 6, 8 \) the photon propagator possesses the same Lorentz tensor structure as in (22) and its gauge dependent tensor has a scalar factor of \( (k^2)^{d/2} \) in the denominator [33]. Therefore, the expression for the skeleton (11) can also be used to construct the gauge dependence in \( d = 6 \) dimensions. However, the eight-dimensional QED Lagrangian features interactions quartic in the field strength, which might contribute gauge dependent terms. So additional tree-level identities might be required.

A further extension of our results might include non-linear gauges. A discussion of the cancellation identities of QED in the ‘t Hooft-Veltman gauge [34] will follow elsewhere.

From the combinatorial proof of the Ward identities, [1, 2, 3, 4, 5, 6] it is reasonable to expect similar cancellations for the quark propagator in QCD. However, one can not expect a linear Dyson-Schwinger equation to describe the gauge dependence, rather, we anticipate that the scalar propagator of the skeleton graph obtains ghost self-energy insertions and that the ghost-gluon vertex induces additional skeletons, which potentially relate to the appearance of higher-order Casimir operators.
Another exciting project will be to investigate cancellation identities in the context of massive gauge bosons and to examine the role of the Goldstone and Higgs bosons in models with spontaneously broken symmetry. However, these questions are clearly beyond the scope of this letter and deserve further investigation.

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