Improved Measurements of Color-Suppressed Decays

\(B^0 \rightarrow D^0\pi^0, D^0\eta\) and \(D^0\omega\)

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We present preliminary improved measurements of the branching fractions of the color-suppressed decays $B^0 \rightarrow D^0 h^0$ where $h^0$ represents the three light neutral mesons $\pi^0$, $\eta$ and $\omega$. The measurements are based on a data sample of 140 fb$^{-1}$ collected at the $\Upsilon(4S)$ with the Belle detector at the KEKB energy-asymmetric $e^+e^-$ collider, corresponding to seven times the luminosity of the previous Belle measurements.
I. INTRODUCTION

The weak decays $B^0 \to D^{(*)0} h^0$ [1], where $h^0$ represents a light neutral meson, are expected to proceed predominantly through internal spectator diagrams, as illustrated in Fig. 1. The color matching requirement between the quarks from the virtual $W^-$ and the other quark pair results in these decays being “color-suppressed” relative to decays such as $B^0 \to D^{(*)} h^-$, which proceed through external spectator diagrams.

Previous measurements of $B^0$ decays into $D^{(*)0} \pi^0$, $D^0 \eta$, $D^0 \omega$, and $D^0 \rho^0$ by the Belle collaboration [2, 3], and of $B^0$ into $D^{(*)0} \pi^0$ by the CLEO collaboration [4], and of $B^0$ decays into $D^{(*)} \pi^0$, $D^{(*)0} \eta$, $D^{(*)0} \omega$, $D^0 \eta'$ by the BaBar collaboration [5] indicate color suppressed branching fractions in the approximate range $(2–4) \times 10^{-4}$. This is substantially in excess of theoretical expectations from “naive” factorization models [6–12] in the range $(0.3–1.7) \times 10^{-4}$.

Several approaches to achieving a better theoretical description [8, 9, 13, 14] have been developed. They extend upon the factorization approach with consideration of final state interactions and consequent simultaneous treatment of isospin amplitudes of color-suppressed and color-allowed decays. The possibility that similar effects could have dramatic implications on the measurement potential of direct $CP$ violation asymmetries in charmless decays, together with some degree of discrepancy between the prior Belle [2] and BaBar [5] measurements provide strong motivation for more precise measurements of the color-suppressed decays.

In this paper we report improved branching fraction measurements of $B^0$ decays into $D^0 \pi^0$, $D^0 \eta$, $D^0 \omega$. The measurements are based on a 140 fb$^{-1}$ data sample, which contains 152 million $B\bar{B}$ pairs, collected with the Belle detector at the KEKB asymmetric-energy $e^+e^-$ (3.5 on 8 GeV) collider [15] operating at the $\Upsilon(4S)$ resonance. This corresponds to seven times the luminosity of the previous Belle measurements [2] and almost twice that of the earlier BaBar measurements [5].

The Belle detector is a large-solid-angle magnetic spectrometer that consists of a three-layer silicon vertex detector (SVD), a 50-layer central drift chamber (CDC), an array of aerogel threshold Čerenkov counters (ACC), a barrel-like arrangement of time-of-flight scintillation counters (TOF), and an electromagnetic calorimeter comprised of CsI(Tl) crystals (ECL) located inside a super-conducting solenoid coil that provides a 1.5 T magnetic field. An iron flux-return located outside of the coil is instrumented to detect $K_L^0$ mesons and to identify muons (KLM). The detector is described in detail elsewhere [16].
II. EVENT SELECTION

Color-suppressed $\bar{B}^0$ meson decays are reconstructed from candidate $D^0$ mesons that are combined with light neutral meson candidates $h^0$. The $D^0$ mesons are reconstructed in three decay modes: $K^-\pi^+$, $K^-\pi^0$, and $K^-\pi^+\pi^-\pi^0$ while the light neutral mesons $h^0$ are reconstructed in the decay modes: $\pi^0 \rightarrow \gamma\gamma$, $\eta \rightarrow \gamma\gamma$, $\eta \rightarrow \pi^+\pi^-\pi^0$ and $\omega \rightarrow \pi^+\pi^-\pi^0$. The invariant masses at each stage of the decay chains are required to be consistent within $2.5 - 3\sigma$ mass resolution or natural width windows around the nominal masses of the assumed particle types. Vertex and mass constrained fits are performed for decays with charged products such as the three $D^0$ decays and $\eta \rightarrow \pi^+\pi^-\pi^0$; mass constrained fits are performed on the $\pi^0 \rightarrow \gamma\gamma$ and $\eta \rightarrow \gamma\gamma$ candidates; and vertex constrained fits are performed on $\omega \rightarrow \pi^+\pi^-\pi^0$ candidates due to the large natural width of the $\omega$ meson. These kinematic fits result in improved energy and momenta of the candidate mesons.

Charged tracks are required to have impact parameters within $\pm 5 \text{ cm}$ of the interaction point along the positron beam axis and within $1 \text{ cm}$ in the transverse plane. Each track is identified as a kaon or pion according to a likelihood ratio derived from the responses of the TOF and ACC systems and energy loss measurements from the CDC. The likelihood ratio is required to exceed 0.6 for kaon candidates. This requirement is 88% efficient for kaons with a misidentification rate for pions of 8.5%.

The photon pairs that constitute $\pi^0$ candidates are required to have energies greater than 50 MeV and an invariant mass within a $\pm 3\sigma$ ($\sigma = 5.4 \text{ MeV}/c^2$) mass window around the nominal $\pi^0$ mass.

Candidate $\eta$ mesons that decay to $\gamma\gamma$ are required to have photon energies $E_\gamma$ greater than 100 MeV. In addition the energy asymmetry $\frac{|E_{\gamma 1} - E_{\gamma 2}|}{E_{\gamma 1} + E_{\gamma 2}}$, is required to be less than 0.9. The $\eta$ candidates are required to have invariant masses within $2.5\sigma$ mass windows of the nominal mass, where $\sigma = 10.6 \text{ MeV}/c^2$ for the $\eta \rightarrow \gamma\gamma$ mode and $3.4 \text{ MeV}/c^2$ for the $\eta \rightarrow \pi^+\pi^-\pi^0$ mode. If the photons that comprise the $\eta \rightarrow \gamma\gamma$ candidate are found to contribute to any $\pi^0 \rightarrow \gamma\gamma$ the candidate is excluded. The $\pi^0$ decay products of the $\eta \rightarrow \pi^+\pi^-\pi^0$ and $\omega \rightarrow \pi^+\pi^-\pi^0$ candidates are required to have CM momentum greater than 200 and 500 MeV, respectively. The $\omega$ candidates are required to have invariant masses within $\pm 3\Gamma$ of the nominal mass value, where $\Gamma$ is the natural width of $8.9 \text{ MeV}/c^2$.

Invariant masses of the $D^0$ candidates are required to be within $\pm 2\sigma$ of the nominal mass where $\sigma$ is 8, 12 and 5 MeV/c$^2$ for the $K^-\pi^+$, $K^-\pi^+\pi^0$, and $K^-\pi^+\pi^+\pi^-$ modes respectively. The CM momentum of the $\pi^0$ in the $K^-\pi^+\pi^0$ mode is required to be greater than 400 MeV.

III. $\bar{B}$ RECONSTRUCTION

The $\bar{B}^0$ candidates are reconstructed from combinations of $D^0$ and $h^0$ using the improved energy and momenta resulting from the vertex and mass constrained fits.

Two kinematic variables are used to distinguish signal candidates from backgrounds: the beam-energy constrained mass $M_{\text{bc}} = \sqrt{(E_{\text{beam}}^* - |\sum \vec{p}_i|^2)^2}$ and energy difference $\Delta E = \sum E_{\gamma i} - E_{\text{beam}}^*$ where $E_{\text{beam}}^*$ is the CM energy, and $E_{\gamma i}^*$, $\vec{p}_i^*$ are the CM energy and momenta, respectively, which are summed over the $D^0$ and $h^0$ meson decay candidates.

The resolution of $M_{\text{bc}}$ is approximately 3 MeV/c$^2$ for all modes, dominated by the beam energy spread, whereas the $\Delta E$ resolution varies substantially among modes depending particularly on the number of $\pi^0$ in the final state. Candidates within the broad region
|ΔE| < 0.25 GeV and 5.2 GeV/c² < M_{bc} < 5.3 GeV/c² are selected for further consideration. Where more than one candidate is found in a single event the one with the smaller $\sum \chi_i^2/N_i$ is chosen, where $\chi_i^2$ and the number of degrees of freedom $N_i$ are obtained from the kinematic fits to the $D^0$ and $h^0$.

A common $M_{bc}$ signal region of 5.27 GeV/c² < $M_{bc}$ < 5.29 GeV/c² is used for all final states. The signal region definitions in $\Delta E$ are mode dependent with $|\Delta E| < 0.05$ GeV for $\omega \rightarrow \pi^+\pi^-\pi^0$ and $\eta \rightarrow \pi^+\pi^-\pi^0$ modes, and $|\Delta E| < 0.08$ GeV for $\pi^0 \rightarrow \gamma\gamma$ and $\eta \rightarrow \gamma\gamma$ modes. The event yields and efficiencies presented in the following sections correspond to these signal regions.

IV. CONTINUUM SUPPRESSION

At energies close to the $\Upsilon(4S)$ resonance the production cross section of $e^+e^- \rightarrow q\bar{q}$ ($q = u, d, s, c$) is approximately three times that of $B\bar{B}$ production, making continuum background suppression essential in all modes. The jet-like nature of the continuum events allows event shape variables to discriminate between them and the more spherical $B\bar{B}$ events.

The discrimination power of seven event shape variables is combined into a single Fisher discriminant [17] whose variables include the angle between the thrust axis of the $B$ candidate and the thrust axis of the rest of the event ($\cos \theta_T$), the sphericity variable, and five modified Fox-Wolfram moments [17].

Monte Carlo event samples of continuum $q\bar{q}$ events and signal events for each of the final states considered are used to construct probability density functions (PDFs) for the Fisher discriminant [17] and $\cos \theta_B$, where $\theta_B$ is the angle between the $B$ flight direction and the beam direction in the $\Upsilon(4S)$ rest frame. The products of the PDFs for these two variables give signal and continuum likelihoods $L_s$ and $L_{q\bar{q}}$ for each candidate, allowing a selection to be applied to the likelihood ratio $L = L_s/(L_s + L_{q\bar{q}})$.

Monte Carlo studies of the signal significance $N_s/\sqrt{N_s + N_b}$, where $N_s$ and $N_b$ are signal and background yields (using signal branching fractions from previous measurements), as a function of a cut on the likelihood ratio $L$ indicate a rather smooth behavior. Although the optimum significance is generally in the range 0.6-0.7, a looser cut of $L > 0.5$ is applied for all modes in order to reduce systematic uncertainties.

For the $B^{0} \rightarrow D^0\omega$ mode the polarized nature of the $\omega$ allows additional discrimination against backgrounds to be achieved with an additional requirement of $|\cos \theta_{hel}| > 0.3$, where the helicity angle $\theta_{hel}$ is defined as the angle between the $B$ flight direction in the $\omega$ rest frame and the vector perpendicular to the $\omega$ decay plane in the $\omega$ rest frame.

V. BACKGROUNDS FROM OTHER $B$ DECAYS

Significant background contributions arise both from color favored decays and from contributions from other color suppressed decays (crossfeed) $B^0 \rightarrow D^{*0}h^0$. Some backgrounds have the same final state as the signal while others mimic signal due to missing or extra particles.

Generic Monte Carlo samples of $B\bar{B}$ and continuum $q\bar{q}$ are used to study the background contributions in the $M_{bc}$ and $\Delta E$ distributions. The $B\bar{B}$ event sample excludes the color suppressed modes under investigation and associated $D^{*0} h^0$ modes. These signal modes for each of the decay chains considered and the corresponding $D^{*0} h^0$ decays are generated and
reconstructed separately. They are used to estimate the crossfeed contributions to the other modes using the branching fractions measured here and by the BaBar collaboration [5]. A combined generic Monte Carlo sample weighted according to the effective production cross sections and selection efficiencies of $q\bar{q}$ and $B\bar{B}$ is also used.

Figures 2, 3 and 4 show the $M_{bc}$ and $\Delta E$ distributions after application of all selection requirements and with the $\Delta E$ signal requirement applied for the $M_{bc}$ distributions (a) and the signal requirement $5.27\text{ GeV}/c^2 < M_{bc} < 5.29\text{ GeV}/c^2$ applied for the $\Delta E$ distributions (b). The $\Delta E$ signal requirements used are $|\Delta E| < 0.08\text{ GeV}$ for $D^0\pi^0$ mode, $-0.08\text{ GeV} < \Delta E < 0.05\text{ GeV}$ for $D^0\eta$, and $|\Delta E| < 0.05\text{ GeV}$ for $D^0\omega$. These regions are indicated by vertical dashed lines on the figures.

The dominant crossfeed contributions to the $D^0h^0$ decays are found to arise from the corresponding $D^{*0}h^0$ decays. These contributions peak at same $M_{bc}$ as the signal but are shifted to the lower side in $\Delta E$. As can be seen from the figures, the crossfeed contribution is substantial in the region $-0.25\text{ GeV} < \Delta E < -0.10\text{ GeV}$ but quite small in the signal region. Within the signal region the fraction of crossfeed is less than 10% of the observed yield in all cases.

For the $\bar{B}^0 \to D^0\pi^0$ mode the color allowed $B^- \to D^{(*)0}\rho^-$ modes are found to be the dominant backgrounds. Non-reconstructed soft $\pi^0$ from $D^{(*)0} \to D^0\pi^0$, photons from $D^{*0} \to D^0\gamma$ and $\pi^-$ from $\rho^- \to \pi^-\pi^0$ produce the same final state as the signal. However the missing particles cause a shift in $\Delta E$ with a broad peak centered at approximately $\Delta E = -0.2\text{ GeV}$. In order to reduce contributions from this background, events that contain $B$ candidates reconstructed as $B^- \to D^{(*)0}\rho^-$ within the signal region $5.27\text{ GeV} < M_{bc} < 5.29\text{ GeV}$ and $|\Delta E| < 0.1\text{ GeV}$ are rejected. This requirement reduces the color allowed
contribution in the region $-0.25 \text{GeV} < \Delta E < -0.10 \text{GeV}$ by about 60% it does little to reduce contributions in the signal region, but remains useful to facilitate background modelling. The $M_{bc}$ distribution of these backgrounds is found to contribute at and slightly below the the $M_{bc}$ signal region.

VI. DATA MODELLING AND SIGNAL EXTRACTION

Independent unbinned extended maximum likelihood fits to the $M_{bc}$ and $\Delta E$ distributions are performed to obtain the signal yields. The yields from the $M_{bc}$ fits are used to extract the branching fractions, while the yields from the $\Delta E$ fits are used to cross-check the results. In most cases the shapes of the signal and background component distributions in $M_{bc}$ and $\Delta E$ are obtained from fits to MC samples.

The signal models used are the same for all modes, with the $M_{bc}$ signals modelled with a Gaussian function and the $\Delta E$ signals with an empirical formula that accounts for the asymmetric calorimeter energy response, known as the Crystal ball line shape [18], added to a Gaussian function of the same mean. The signal models are represented in Figures 2-4 by the dotted lines. Fits of the $\Delta E$ distributions to signal Monte Carlo for each final state are used to obtain the signal shape parameters; all the $M_{bc}$ signal shape parameters are allowed to float in fits to data.

The crossfeed contributions in $M_{bc}$ and $\Delta E$ are studied using a combination of signal Monte Carlo samples from all other color suppressed modes, weighted according to the branching fractions obtained here or from the Babar measurements [5]. Smoothed histograms obtained from this combined sample are used as estimates of the crossfeed contri-
FIG. 4: Distributions of (a) $M_{bc}$ and (b) $\Delta E$ for $B^0 \to D^0 \omega$. Points with error bars represent the data, the solid line shows the result of the fit and the dotted line represents the signal contribution. The vertical dashed lines represent the signal region. For (a) the dashed-dotted line shows the continuum-like background contribution, with peaking background contributions represented by the small dashed line. For (b) the dashed-dotted lines show the sum of $B$ background and continuum contributions.

In the $M_{bc}$ case the $\Delta E$ signal region requirement results in very small crossfeed contributions, which are fixed at the Monte Carlo expectation. For $\Delta E$ there are considerable contributions in the region $-0.25 \text{ GeV} < \Delta E < -0.10 \text{ GeV}$; the normalization of this component is allowed to float in the fit.

Continuum like backgrounds in the $M_{bc}$ fits are modelled by an empirical threshold function known as the ARGUS function [19]. The small peaking background contributions are modelled by a Gaussian of mean and width and normalization obtained by a fit to the $B \bar{B}$ background Monte Carlo $M_{bc}$ distribution, using an ARGUS function plus a Gaussian. A systematic uncertainty of 50% is assigned to the determination of this small background distribution. This treatment allows the vast majority of the background to be simply modelled with the ARGUS shape leaving a small but less well known peaking background component that represents the deviation from the ARGUS shape.

In fits to data $M_{bc}$ distributions the ARGUS background function parameters are fixed to the values obtained from fits to combined Monte Carlo $B \bar{B}$ and continuum background samples. The signal parameters are free, as are the normalizations of signal and background. The small peaking background and crossfeed contributions are fixed at their expected values.

The $\Delta E$ background distributions in the $B^0 \to D^0 \eta$ and $B^0 \to D^0 \omega$ are modelled using smoothed histograms obtained from a combined continuum and generic $B \bar{B}$ Monte Carlo sample.

For the $B^0 \to D^0 \pi^0$ mode, the shapes of the $\Delta E$ distribution arising from $B \bar{B}$ and continuum background are very different, necessitating separate modelling. The continuum shape is modelled with a first order polynomial with slope obtained from fits to the continuum Monte Carlo sample. The shape of the $B \bar{B}$ background is modelled with a Gaussian function plus a second order polynomial, with parameters determined from a
fit to the generic $B\bar{B}$ Monte Carlo sample. In fits to data the large peak in the region $-0.25 \text{GeV} < \Delta E < -0.10 \text{GeV}$ that arises principally from the color allowed $B^- \rightarrow D^{(*)0}\rho^-$ decays is found to be broader than the Monte Carlo expectation, thus all parameters of this color allowed Gaussian are allowed to float in the fit. The normalizations of the contributions from the remainder of the $B\bar{B}$ background, the continuum and the signal are also floated in the fit, with the small crossfeed fixed as discussed above.

The results of the $M_{bc}$ and $\Delta E$ fits for the combined modes are presented in Figures 2, 3 and 4.

TABLE I: Measured signal region yields and MC estimates of signal region contributions for $\bar{D}^0 \rightarrow D^0\eta^0$ for the combined $D^0$ subdecay modes and the individual $D^0$ subdecay modes. The numbers of signal events $N_{sig}$ and continuum like events $N_{bkg}$ obtained from the $M_{bc}$ fit are listed together with their statistical uncertainties. MC estimates of the contributions from peaking $B$ background $N_{pkb}$ and crossfeeds from other color suppressed modes $N_{xrs}$ are listed together with their systematic uncertainties.

| Mode                  | $N_{sig}$   | $N_{bkg}$   | $N_{pkb}$   | $N_{xrs}$   |
|-----------------------|-------------|-------------|-------------|-------------|
| $D^0\pi^0$            | 637.1 ± 33.9 | 613.4 ± 25.6 | 21.1 ± 10.5 | 25.9 ± 6.5  |
| $D^0(K\pi)\pi^0$     | 216.6 ± 17.1 | 94.3 ± 10.2  | 6.1 ± 3.0   | 6.9 ± 1.7   |
| $D^0(K\pi\pi^0)\pi^0$| 184.5 ± 17.6 | 191.9 ± 14.0 | 4.8 ± 2.4   | 7.6 ± 1.9   |
| $D^0(K\pi\pi\pi)\pi^0$| 260.0 ± 21.7 | 322.1 ± 18.6 | 13.2 ± 6.6  | 11.5 ± 2.9  |
| $D^0\eta(\gamma\gamma)$ | 161.3 ± 16.8 | 135.6 ± 12.6 | 4.5 ± 2.2   | 10.7 ± 2.7  |
| $D^0(K\pi)\eta(\gamma\gamma)$ | 59.8 ± 8.9 | 21.0 ± 4.8   | 0.0 ± 0.0   | 3.7 ± 0.9   |
| $D^0(K\pi^0)\eta(\gamma\gamma)$ | 51.7 ± 8.7 | 38.4 ± 6.3   | 4.1 ± 2.1   | 2.9 ± 0.7   |
| $D^0(K\pi\pi\pi)\eta(\gamma\gamma)$ | 70.6 ± 10.7 | 72.5 ± 9.4   | 2.5 ± 1.3   | 4.1 ± 1.0   |
| $D^0\eta(\pi^0\pi\pi)$ | 68.5 ± 10.6 | 41.6 ± 6.3   | 1.2 ± 0.6   | 2.0 ± 0.5   |
| $D^0(K\pi)\eta(\pi^0\pi\pi)$ | 21.4 ± 5.3 | 7.2 ± 2.6    | 0.8 ± 0.4   | 0.5 ± 0.1   |
| $D^0(K\pi\pi^0)\eta(\pi^0\pi\pi)$ | 16.3 ± 5.1 | 12.6 ± 3.5   | 1.4 ± 0.7   | 0.8 ± 0.2   |
| $D^0(K\pi\pi\pi)\eta(\pi^0\pi\pi)$ | 31.7 ± 6.8 | 21.6 ± 4.5   | 0.4 ± 0.2   | 0.7 ± 0.2   |
| $D^0\eta(\pi^0\pi\pi)$ | 233.1 ± 19.9 | 173.9 ± 13.8 | 5.5 ± 2.7   | 12.7 ± 3.2  |
| $D^0\omega(\pi^0\pi\pi)$ | 191.9 ± 17.8 | 154.1 ± 12.1 | 3.4 ± 1.7   | 3.5 ± 0.9   |
| $D^0(K\pi)\omega(\pi^0\pi\pi)$ | 73.5 ± 9.8 | 31.8 ± 5.7   | 3.0 ± 1.5   | 0.8 ± 0.2   |
| $D^0(K\pi\pi^0)\omega(\pi^0\pi\pi)$ | 54.0 ± 8.9 | 43.5 ± 6.2   | 0.0 ± 0.0   | 1.3 ± 0.3   |
| $D^0(K\pi\pi\pi)\omega(\pi^0\pi\pi)$ | 73.2 ± 11.0 | 77.8 ± 8.5   | 1.0 ± 0.5   | 1.4 ± 0.3   |

VII. BRANCHING FRACTION RESULTS
contribute substantially less than the extent of the statistical uncertainty on the signal yield. Both peaking backgrounds and crossfeed contributions in the signal region can be seen to statistically uncertain. The results from the fit sample, with the ∆E signal region requirement applied. The relative uncertainty is given in brackets.

| Mode                  | ε<sub>MC</sub>       | ε<sub>DA/MC</sub> | ε<sub>corr</sub> |
|-----------------------|----------------------|-------------------|-----------------|
| D<sup>0</sup>π<sup>0</sup> | 0.078 ± 0.002(1.9%)  | 0.938 ± 0.048(5.1%) | 0.075 ± 0.004(5.5%) |
| D<sup>0</sup>(Kπ)π<sup>0</sup> | 0.177 ± 0.002(1.4%)  | 0.979 ± 0.045(4.6%) | 0.173 ± 0.008(4.8%) |
| D<sup>0</sup>(Kππ<sup>0</sup>)π<sup>0</sup> | 0.047 ± 0.001(2.9%)  | 0.905 ± 0.044(4.9%) | 0.042 ± 0.002(5.7%) |
| D<sup>0</sup>(Kπππ)π<sup>0</sup> | 0.087 ± 0.001(1.5%)  | 0.979 ± 0.057(5.8%) | 0.085 ± 0.005(6.0%) |
| D<sup>0</sup>η(γγ)     | 0.060 ± 0.001(2.0%)  | 0.989 ± 0.058(5.9%) | 0.061 ± 0.004(6.2%) |
| D<sup>0</sup>(Kπ)η(γγ) | 0.134 ± 0.002(1.6%)  | 1.032 ± 0.057(5.5%) | 0.139 ± 0.008(5.7%) |
| D<sup>0</sup>(Kππ<sup>0</sup>)η(γγ) | 0.038 ± 0.001(2.6%)  | 0.954 ± 0.054(5.7%) | 0.036 ± 0.002(6.2%) |
| D<sup>0</sup>(Kπππ)η(γγ) | 0.064 ± 0.001(1.8%)  | 1.032 ± 0.067(6.5%) | 0.066 ± 0.004(6.7%) |
| D<sup>0</sup>η(π<sup>0</sup>ππ) | 0.044 ± 0.001(2.5%)  | 0.940 ± 0.055(5.9%) | 0.042 ± 0.003(6.4%) |
| D<sup>0</sup>(Kπ)η(π<sup>0</sup>ππ) | 0.096 ± 0.002(1.8%)  | 0.981 ± 0.054(5.5%) | 0.094 ± 0.005(5.8%) |
| D<sup>0</sup>(Kππ<sup>0</sup>)η(π<sup>0</sup>ππ) | 0.028 ± 0.001(3.5%)  | 0.906 ± 0.052(5.7%) | 0.025 ± 0.002(6.7%) |
| D<sup>0</sup>(Kπππ)η(π<sup>0</sup>ππ) | 0.046 ± 0.001(2.1%)  | 0.981 ± 0.064(6.5%) | 0.046 ± 0.003(6.8%) |
| D<sup>0</sup>ω(π<sup>0</sup>ππ) | 0.028 ± 0.001(2.9%)  | 0.885 ± 0.061(6.9%) | 0.025 ± 0.002(7.5%) |
| D<sup>0</sup>(Kπ)ω(π<sup>0</sup>ππ) | 0.060 ± 0.001(2.3%)  | 0.924 ± 0.061(6.6%) | 0.055 ± 0.004(7.0%) |
| D<sup>0</sup>(Kππ<sup>0</sup>)ω(π<sup>0</sup>ππ) | 0.017 ± 0.001(3.8%)  | 0.854 ± 0.058(6.8%) | 0.015 ± 0.001(7.8%) |
| D<sup>0</sup>(Kπππ)ω(π<sup>0</sup>ππ) | 0.032 ± 0.001(2.5%)  | 0.924 ± 0.069(7.4%) | 0.029 ± 0.002(7.8%) |

| Mode                  | D<sup>0</sup>(Kπ)       | D<sup>0</sup>(Kππ<sup>0</sup>) | D<sup>0</sup>(Kπππ)       |
|-----------------------|--------------------------|-------------------------------|----------------------------|
| D<sup>0</sup>π<sup>0</sup> | 2.20 ± 0.17 ± 0.18       | 2.11 ± 0.20 ± 0.24            | 2.75 ± 0.23 ± 0.27         |
| D<sup>0</sup>η(γγ)     | 1.89 ± 0.28 ± 0.18       | 1.73 ± 0.29 ± 0.22            | 2.39 ± 0.36 ± 0.26         |
| D<sup>0</sup>η(π<sup>0</sup>ππ) | 1.69 ± 0.42 ± 0.15      | 1.32 ± 0.41 ± 0.17            | 2.66 ± 0.57 ± 0.26         |
| D<sup>0</sup>ω(π<sup>0</sup>ππ) | 2.55 ± 0.34 ± 0.27      | 1.95 ± 0.32 ± 0.27            | 2.45 ± 0.37 ± 0.29         |

TABLE III: Measured branching fractions for the process $\bar{B}^0 \to D^0 h^0 \times 10^{-4}$ using separate $D^0$ subdecay mode samples, as obtained from the $M_{bc}$ fit. The branching fractions are listed with statistical and systematic uncertainties.

Results of $M_{bc}$ and ∆E fits are consistent; the agreement is typically within 50% of the statistical uncertainty. The results from the $M_{bc}$ fits are found to have a slightly smaller total uncertainty in most cases and are used for the final result. Yields are obtained both from the individual subdecay mode samples and from samples with the three $D^0$ subdecay samples combined. The yields from the one dimensional $M_{bc}$ fits are shown in Table I. Both peaking backgrounds and crossfeed contributions in the signal region can be seen to contribute substantially less than the extent of the statistical uncertainty on the signal yield.
The yields obtained are interpreted as branching fractions using the number of analyzed $B\bar{B}$ events, the product of subdecay fractions from PDG [20] corresponding to the decay of $D^0 h^0$ into the observed final states and the total selection efficiency. The efficiency for each mode is first obtained from signal Monte Carlo samples and then corrected by comparing data and MC predictions for other processes. For the $\pi^0$ reconstruction efficiency the correction is obtained from comparisons of $\eta \rightarrow \pi^0 \pi^0 \pi^0$ to $\eta \rightarrow \gamma \gamma$ and to $\eta \rightarrow \pi^+ \pi^- \pi^0$, for data and Monte Carlo. The MC efficiency, correction factor and corrected efficiency are presented in Table II. The corrections are obtained from the product of correction factors relevant to the final state of each submode.

The branching fraction results for the individual submodes are shown in Table III. The combined submode systematic uncertainties and branching fraction results are shown in Tables IV and V, respectively.

### VIII. SYSTEMATIC UNCERTAINTIES

| Category                        | $D^0 \pi^0$ | $D^0 \eta(\gamma \gamma)$ | $D^0 \eta(\pi^0 \pi \pi)$ | $D^0 \eta D^0 \omega(\pi^0 \pi \pi)$ |
|---------------------------------|-------------|-----------------------------|-----------------------------|-------------------------------------|
| Tracking efficiency             | 2.6         | 2.6                         | 2.6                         | 2.6                                 |
| $h^0$ efficiency                | 2.7         | 4.0                         | 2.6                         | 2.6                                 |
| Kaon efficiency                 | 1.0         | 1.0                         | 1.0                         | 1.0                                 |
| Extra $\pi^0$ efficiency        | 0.4         | 0.4                         | 0.4                         | 0.4                                 |
| Likelihood ratio efficiency     | 3.0         | 3.0                         | 3.0                         | 3.0                                 |
| MC statistics                   | 2.3         | 2.2                         | 2.8                         | 2.4                                 |
| Peaking background              | 1.7         | 1.4                         | 0.9                         | 1.2                                 |
| Crossfeed                       | 1.0         | 1.7                         | 0.7                         | 1.4                                 |
| $\Delta E$ resolution           | 5.0         | 5.0                         | 5.0                         | 5.0                                 |
| Modelling ±1σ variations        | 2.0         | 5.4                         | 0.2                         | 10.6                                |
| Branching Fractions $D^0$, $\pi^0$, $\eta$, $\omega$ | 5.2 | 5.2 | 5.5 | 5.3 | 5.2 |
| Number of $B\bar{B}$ events     | 0.7         | 0.7                         | 0.7                         | 0.7                                 |
| Total (%)                       | 9.5         | 11.1                        | 9.9                         | 14.4                                |

Systematic uncertainties of the combined modes, estimated for the results based on the $M_{bc}$ fits are summarized in Table IV. Uncertainties on the efficiency correction factors relevant to each final state are listed in the Tables together with other uncertainties. For the $M_{bc}$ fit the uncertainty from the peaking background, which is fixed at the MC expectation in the fit, is obtained by propagating a 50% uncertainty on the normalization of this contribution. The crossfeed uncertainty is estimated as 25% of the contribution from this source in the signal regions. This accounts for uncertainties on the branching fractions of the crossfeed contributions and also differences observed between the floated crossfeed contributions in
$\Delta E$ fits and the MC expectation. Uncertainties arising from the background and signal modelling used are estimated from the changes in the yields as a result of ±1σ variations on the model parameters. The total uncertainty is obtained regarding uncertainties from different sources as uncorrelated.

TABLE V: Measured branching fractions for the process $B^0 \rightarrow D^0 h^0 \times 10^{-4}$ using combined $D^0$ subdecay mode samples, as obtained from the $M_{bc}$ fit. The branching fractions are listed with statistical and systematic uncertainties. The $D^0\eta$ result is obtained from a combined sample of $D^0\eta(\gamma\gamma)$ and $D^0\eta(\pi^+\pi^-\pi^0)$.

| Mode                  | Branching fraction ($\times 10^{-4}$) |
|-----------------------|---------------------------------------|
| $D^0\pi^0$            | 2.31 ± 0.12 ± 0.23                    |
| $D^0\eta(\gamma\gamma)$ | 1.77 ± 0.18 ± 0.20                    |
| $D^0\eta(\pi^0\pi\pi)$ | 1.89 ± 0.29 ± 0.20                    |
| $D^0\eta$             | 1.83 ± 0.15 ± 0.27                    |
| $D^0\omega(\pi^0\pi\pi)$ | 2.25 ± 0.21 ± 0.28                   |

IX. CONCLUSION

Improved measurements of the branching fractions of the color-suppressed decays $B^0 \rightarrow D^0\pi^0$, $D^0\eta$ and $D^0\omega$ are presented. The results are consistent with the previous Belle measurements. The total uncertainty of the new results is two to three times smaller than the previous results, mostly due to the seven times larger data sample. However comparing the results with those of BaBar [5] and CLEO [4] indicates an approximately 2σ difference, with all three branching fractions measured here lower than the previous measurements.

All the branching fraction results are similar, in the range $1.8-2.4 \times 10^{-4}$. The large values disfavour theoretical predictions based on naive factorization descriptions and indicate the need for models including final state interaction effects to satisfactorily describe the observations.
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