Effects of pH value and Sintering Temperature on the Structural and Magnetic Properties of Barium Hexaferrites Prepared by Co-Precipitation

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Abstract
Barium hexaferrite (BaFe₁₂O₁₉; M-type; BaM) is an important, cost effective magnetic material for permanent magnet applications. The magnetic properties of the prepared samples, and the purity of the BaM phase depend critically on the synthesis route and experimental conditions. In this study, BaM hexaferrites were prepared by co-precipitation method using two different values of pH for the precursor solutions (11.0 and 12.5), and sintering pellets of the co-precipitates at 860, 920 and 990°C. The prepared samples were characterized using X-ray diffraction and magnetic measurements. X-ray diffraction patterns indicated that the samples prepared with pH = 12.5 consisted of a single BaM phase at all sintering temperatures. However, the patterns of the samples with pH = 11.0 did not reveal the existence of BaM at 860°C, whereas a major BaM phase (86 – 87 wt.%) was observed at 920 and 990°C with a minor α-Fe₂O₃ phase. The thermo magnetic curves confirmed the BaM magnetic phase in the samples. The hysteresis loops of the BaM samples showed characteristics of hard magnetic materials with relatively high saturation magnetization. Analysis of the magnetic data indicated an intrinsic coercivity $H_{ci} \sim 5$ kOe for all samples, and a saturation specific magnetization in the range $σ_s = 56.0 – 66.3$ emu/g, which are suitable for permanent magnet applications. The practical coercivity ($H_{cb}$), residual induction ($B_r$) and maximum energy product ($BH_{max}$) of the samples with pH = 12.5 are higher than those of the samples with pH = 11.0, and the highest magnetic parameters of $H_{cb} = 1871$ Oe, $B_r = 2384$ G, and $(BH)_{max} = 8.92$ kJ/m³ were observed for the sample with pH = 12.5 and sintered at 860°C.

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Introduction
M-type hexaferrite of chemical formula $AFe_{12}O_{19}$ ($A = \text{Ba, Sr, Pb}$) belongs to an important class of magnetic oxides exhibiting a wide range of interesting industrial and technological applications, including permanent magnet, magnetic recording, microwave absorption and microwave devices.\textsuperscript{1-10} This range of applications can be facilitated by controlled tuning of the properties of BaM, which can be achieved by special substitutions for $A^{2+}$ and/or $Fe^{3+}$ ions, and by modifying the synthesis route as described by recent review articles.\textsuperscript{11-13} The improvement of the characteristics of a material for permanent magnet applications involves the simultaneous increase of its coercivity and remnant magnetization. On the other hand, tailoring the properties of the material for magnetic recording involves the control of the coercivity in the range of $1 - 3$ kOe, while maintaining a high remnant magnetization (typically above 20 emu/g).

The method of preparation, the adopted experimental conditions including stoichiometry and sintering temperature, and controlling the particle size distribution of the ceramic powder play important role in determining the magnetic properties of BaM. Recently, the effects of synthesis method (ball milling versus sol-gel method), cationic substitutions, and sintering temperature on the magnetic properties of M-type hexaferrites for permanent magnet applications demonstrated high sensitivity to these experimental parameters.\textsuperscript{14, 15} While low sintering temperatures ($< 1000^\circ\text{C}$) are required for preparing M-type hexaferrites with single domain magnetic particles and enhanced coercivity, it is difficult to prepare a high purity phase by conventional ceramic method or ball milling using such low sintering temperatures, which leads to lower magnetic parameters. Alternatively, researchers have used special substitution scenarios to produce M-type hexaferrites with high coercivities suitable for high quality permanent magnets.\textsuperscript{15-21} However, in several cases, the improvement of the coercivity was accompanied by some drawbacks such as unfavorable decrease of the saturation and remnant magnetizations, the use of expensive rare-earth elements, and elaborate experimental procedures.\textsuperscript{20-24}

Co-precipitation technique was reported to be successful for the preparation of M-type hexaferrites with controlled particle size distribution and enhanced coercivity at low sintering temperatures.\textsuperscript{25-27} The effects of stoichiometry, heat treatment, and pH on the formation of the hexaferrite phase and its magnetic properties were addressed by several researchers.\textsuperscript{28-31} The reported results indicated large variations of the magnetic properties, and sensitivity to the details of the experimental procedures. The observed deterioration of certain magnetic parameters such as the saturation magnetization could be associated with nonmagnetic impurity phases coexisting with the M-type hexaferrite phase, whereas the deterioration of the coercivity could be associated with particle morphology and particle-size distribution. This study is concerned with optimizing the experimental conditions for the production of high-quality BaM ($\text{BaFe}_{12}O_{19}$) hexaferrites by coprecipitation of stoichiometric solutions of iron and barium nitrates. The effects of pH and heat treatment on the phase purity of BaM, and its structural and magnetic properties are investigated.

Experimental Techniques
Co-precipitation method was adopted for the preparation of BaM hexaferrites using high-purity ($\geq 99\%$) $\text{Ba(NO}_3)_2$ and $\text{Fe(NO}_3)_3\cdot 9\text{H}_2\text{O}$ starting powders. Stoichiometric amounts of the starting powders were used to prepare the starting solutions by dissolving the metal nitrates in distilled water. The solutions were mixed, and the ferrite precursor was precipitated from this mixture by adding 6M NaOH solution drop wise with the pH of the solution adjusted to 11.0 or 12.5. The solution containing the precipitate was centrifuged at 7000rpm for 2 min., and the powder precipitate was separated and washed with D.I. water ten times. The powder was then dried at $100^\circ\text{C}$ for (4-8) hrs. Disk-shaped pellets were prepared using a hydraulic press and a force of 50 kN, and sintered in air at 860, 920 and 990$^\circ\text{C}$ for 2 h. The synthesized samples were characterized using X-ray diffraction (XRD), and vibrating sample magnetometry (VSM).

Results and Discussion
XRD Results
Fig. 1 shows XRD patterns for all samples prepared at pH = 11.0 and 12.5, and sintered at different temperatures. The pattern of the sample with pH = 11.0 and sintered at 860$^\circ\text{C}$ indicated the presence of a major $\alpha-\text{Fe}_2\text{O}_3$ oxide phase (JCPDS: 01-079-1741), and other unidentified peaks (labelled by $\beta$).
indicated the presence of a secondary Ba-containing minor phases. However, XRD patterns for the samples with pH = 11.0 and sintered at 920°C and 990°C revealed the evolution of a major BaM hexaferrite phase (JCPDS: 00-043-0002), in addition to a small amount of α-Fe$_2$O$_3$ phase represented by the weak peaks corresponding to its structural reflections. On the other hand, XRD patterns of the samples prepared at pH = 12.5 indicated the presence of a single BaM phase at all sintering temperatures, without any additional secondary phases. By comparing the patterns of the samples prepared at pH = 11.0, we notice the sensitivity of the formation of BaM phase to the sintering temperature. However, with pH = 12.5, the formation temperature of a pure BaM phase was significantly lowered, where a pure BaM phase was observed at 860°C without any secondary phase, indicating the sensitivity of the purity of BaM phase to the pH value. In comparison, the coexistence of a secondary phase with the major BaM phase in samples sintered at 920°C, and with pH = 12.0 and 12.5, was reported in a previous study. The higher quality of our samples in terms of phase purity could be attributed to adopting different experimental conditions such as the starting materials (iron and barium nitrates rather than iron and barium chlorides), and Fe/Ba ratio (12 rather than 10 – 11). These results indicate that all experimental conditions, starting materials, pH value, heat treatment, and chemical stoichiometry, need to be optimized for the production of high quality M-type hexaferrites.

Fig. 1: XRD patterns for the samples prepared with the indicated pH value and sintering temperature. The peaks in the top pattern correspond to α-Fe$_2$O$_3$ phase (α), whereas those corresponding to the unidentified phase are labelled by (β). The JCPDS standard patterns of BaM (00-043-0002) and α-Fe$_2$O$_3$ (01-079-1741) are included for comparison.

Fig. 2: XRD pattern with Rietveld refinement for the sample with pH = 11.0 and sintered at 920°C. The blue line under the pattern represents the difference between the experimental data and theoretical fit. The standard patterns for BaM and α-Fe$_2$O$_3$ phase are shown for comparison.
To determine the refined structural parameters and the weight percent (wt.%) of the phases in the samples, the XRD patterns were refined by Rietveld analysis using Full Prof software. Fig. 2 shows a representative Rietveld-refined XRD pattern for the sample with pH = 11.0 sintered at 920°C. The refined atomic parameters used to simulate the experimental pattern are shown in Table 1. The quality of fit for all patterns was very good as indicated by comparing the experimental data (black circles) with the theoretical pattern (red line), and by the horizontal difference curve (blue line representing the difference between the experimental data and the theoretical fit). The high quality of the fit was also indicated by the low values of the reliability factors (Bragg ($R_b$) and structure factor ($R_f$) reliability factors in Table 2). Table 2 shows the refined lattice parameters (a and c), cell volume (V), and X-ray density ($\rho_x$), whereas Table 3 shows the wt.% of phases in the samples containing BaM phase.

The refined lattice parameters $a = (5.8889 \pm 0.0032)$ Å and $c = (23.199 \pm 0.010)$ Å of the BaM phase in all samples are in good agreement with the reported values for BaM hexaferrites[32, 33]. Also, the refined X-ray density of $\rho_x = (5.299 \pm 0.007)$ g/cm is in good agreement with reported values for BaM samples. The results also indicated that the samples with pH = 11.0 and sintered at 920°C and 990°C consisted of a major BaM phase (87 wt.% and 86 wt.%, respectively), in addition to a secondary $\alpha$-$\text{Fe}_2\text{O}_3$ phase (13 wt.% and 14 wt.%, respectively), whereas the samples with pH = 12.5 consisted of a pure BaM phase at all sintering temperatures. These results confirm our qualitative discussion of the XRD patterns in the first paragraph of this section.

**Table 1: The refined atomic parameters of the BaM phase used to simulate the experimental pattern in Fig. 2**

| Atom | Site | Symmetry | x/a | y/b | z/c |
|------|------|----------|-----|-----|-----|
| Ba   | 2d   | -6m2     | 2/3 | 1/3 | 1/4 |
| Fe1  | 2a   | -3m.     | 0   | 0   | 0   |
| Fe2  | 2b   | -6m2     | 0   | 0   | 1/4 |
| Fe3  | 4f   | 3m.      | 1/3 | 2/3 | 0.02755 |
| Fe4  | 4f   | 3m.      | 1/3 | 3/2 | 0.19052 |
| Fe5  | 12k  | .m.      | 1/6 | 1/3 | 0.89151 |
| O1   | 4e   | 3m.      | 0   | 0   | 0.15427 |
| O2   | 4f   | 3m.      | 1/3 | 2/3 | 0.9467 |
| O3   | 6h   | mm2      | 1/6 | 1/3 | 1/4 |
| O4   | 12k  | .m.      | 1/6 | 1/3 | 0.0518 |
| O5   | 12k  | .m.      | 1/2 | 1   | 0.14956 |

**Table 2: BaM lattice constant and cell volume, X-ray density, and reliability factors**

| Sample     | a (Å) | c (Å) | V (Å³) | $\rho_x$ (g/cm³) | $R_b$ | $R_f$ |
|------------|-------|-------|--------|-----------------|-------|-------|
| pH11@920   | 5.8885| 23.200| 696.69 | 5.298           | 2.82  | 2.33  |
| pH11@990   | 5.8890| 23.202| 696.86 | 5.297           | 2.64  | 2.23  |
| pH12.5@860 | 5.8857| 23.189| 695.68 | 5.306           | 3.38  | 2.66  |
| pH12.5@920 | 5.8913| 23.205| 697.50 | 5.292           | 2.94  | 2.62  |
| pH12.5@990 | 5.8901| 23.201| 697.07 | 5.296           | 2.32  | 1.98  |

**Table 3: Weigh ratios of BaM and $\alpha$-$\text{Fe}_2\text{O}_3$ phases determined by the refinement of the XRD data of each sample**

| pH | 11.0 | 12.5 |
|----|------|------|
| T (°C) | 920 | 990 | 860 | 920 | 990 |
| BaM wt.% | 87 | 86 | 100 | 100 | 100 |
| $\alpha$-$\text{Fe}_2\text{O}_3$ wt.% | 13 | 14 | 0 | 0 | 0 |
Magnetic Measurements

Isothermal Magnetization

The magnetic properties of the samples were measured by VSM at room temperature in a magnetic field up to 10 kOe. The hysteresis loops of all samples are shown in Fig. 3. The hysteresis loop of the sample with pH = 11.0 sintered at 860°C exhibited almost a linear behaviour, with a weak magnetization (~ 1 emu/g at the maximum field of 10 kOe), and a small opening in the central region. This result is consistent with the structural analysis, where the magnetic behaviour is attributed to the weakly ferromagnetic behaviour of α-Fe₂O₃ exhibiting canted antiferromagnetic structure at room temperature. Similar behaviour with maximum magnetization of 0.31 – 1.30 emu/g was observed in commercial α-Fe₂O₃ powders. However, the hysteresis loops of all other samples are wide, and demonstrated tendency toward saturation at high fields, which is characteristic of the behaviour of hard magnetic materials. These results are also consistent with the XRD results which revealed the presence of a major BaM phase in these samples.

The saturation specific magnetization (σₛ) of each sample was obtained from the Law of Approach to Saturation in the high-field range. In the field range H = 8.5 – 10 kOe, the specific magnetization (σ) was found to obey the relation

\[ \sigma = \sigma_s \left(1 - \frac{B}{H^2}\right) \]

where B is a constant representing the magnetocrystalline anisotropy, indicating that the magnetization behaviour can be described by the magnetocrystalline anisotropy contribution. The values of σₛ obtained from the linear fit to the σ vs. 1/H² plots (not shown for brevity), as well as the remnant specific magnetization (σᵣ) and the intrinsic coercivity (Hᵣ) obtained from the hysteresis loops are listed in Table 4. In addition, the values of the magnetocrystalline anisotropy field (Hₐ), and the first anisotropy constant (K₁) for the samples containing a major BaM phase were determined from the constant B using the relation

\[ B = \frac{H_a^2}{15} = \frac{1}{15} \left(\frac{2K_1}{\sigma_s}\right)^2 \]...

The values of these magnetic parameters are also listed in Table 4.

Table 4: Saturation magnetization (σₛ), remanence(σᵣ), squareness ratio (σᵣ/σₛ), intrinsic coercivity (Hᵣ), magnetic anisotropy field (Hₐ), and first anisotropy constant (K₁) for the samples containing a major BaM phase

| pH  | Sintering Temperature | σₛ (emu/g) | σᵣ (emu/g) | σᵣ/σₛ | Hᵣ (kOe) | Hₐ (kOe) | K₁ (10⁶erg/cm³) |
|-----|----------------------|------------|------------|--------|-----------|-----------|--------------|
| 11.0| 920°C                | 56.0       | 29.8       | 0.53   | 5.33      | 12.4      | 1.84         |
|     | 990°C                | 58.0       | 31.2       | 0.54   | 5.03      | 12.4      | 1.91         |
| 12.5| 860°C                | 58.6       | 33.1       | 0.56   | 5.14      | 13.0      | 2.02         |
|     | 920°C                | 66.3       | 35.0       | 0.53   | 5.17      | 12.6      | 2.21         |
|     | 990°C                | 65.9       | 34.7       | 0.53   | 4.93      | 12.4      | 2.16         |

The values of σₛ and σᵣ for the samples prepared with pH = 12.5 are significantly higher than those of the samples prepared with pH = 11.0 at all sintering temperatures. The improvement of σₛ for the samples prepared with pH = 12.5 is attributed to the higher purity of the BaM phase in these samples as demonstrated by their XRD patterns. The maximum
value of $\sigma_s = 66.3 \text{ emu/g}$ and $\sigma_r = 35.0 \text{ emu/g}$ for the sample with pH = 12.5 and sintered at 920°C are somewhat higher than $\sigma_s = 62.2 \text{ emu/g}$ and $\sigma_r = 33.6 \text{ emu/g}$ recently reported for BaM sample prepared by ball milling and sintered at 1100°C.\textsuperscript{14} Also, the highest saturation magnetization obtained by our group is close to the maximum value of 68 emu/g recently reported for BaM sample prepared by coprecipitation with pH = 13 and sintered at 1000°C.\textsuperscript{39} However, the observed intrinsic coercivity of $H_i = 5.13 \pm 0.20$ kOe for all samples in this study is significantly higher than 2.67 – 3.61 kOe or 2.40 – 4.40 kOe reported in the two above mentioned studies, respectively. Considering that the coercivity is an important parameter of hard magnetic materials, the results demonstrate that our method provided a high purity BaM hexaferrite at relatively low sintering temperatures for permanent magnet applications. Low sintering temperatures are important to obtain single domain particles by avoiding particle growth at higher sintering temperatures. The single domain nature of the prepared samples is evidenced by squareness ratio $\sigma_{rs}$ (Table 4), being slightly higher than the value of $\sim 0.5$ characteristics of an assembly of randomly oriented, single-domain magnetic particles (multi-domain particles exhibit a squareness ratio $< 0.5$).

The magnetocrystalline anisotropy field for the samples fluctuated by $\sim 2\%$ around the average value ($H_a = 12.7\pm 0.3$ kOe), whereas the first anisotropy constant $K_1$ increased at pH = 12.5 by about 20\% (from $1.84\times 10^6$ to $2.21\times 10^6$ erg/cm$^3$) at sintering temperature 920°C, and by about 13\% (from $1.91\times 10^6$ to $2.16\times 10^6$ erg/cm$^3$) at sintering temperature 990°C. The lower values of $K_1$ for the samples prepared at pH = 11.0 do not necessarily indicate a reduction of the magnetocrystalline anisotropy of the BaM phase in these samples, but rather, could be attributed to the lower saturation magnetization due to the impurity phases. The observed values of the anisotropy field and first anisotropy constant are in good agreement with values reported for BaM prepared by ball milling and sol-gel methods.\textsuperscript{14}

Further analysis of the magnetization data involves determination of the maximum energy product, and investigating the linearity of the B-H curve in the second quadrant (demagnetization curve) of the hysteresis loop. These are two key quality parameters for permanent magnet applications.\textsuperscript{40} The magnetic induction $B = H + 4\pi M$, where the magnetization($M$) is the product of the specific magnetization ($\sigma$) and the density($M = \rho \times \sigma$). Fig. 4 shows representative hysteresis loops of B and $4\pi M$ for the samples sintered at 920°C. The portion of the B-H curve in the second quadrant is shown in Fig. 5 for all samples. The linear behaviour indicates stability of these materials against stray fields in motor operation at relatively high temperatures.\textsuperscript{41} The practical coercivity $H_{c_B}$ (also called the coercivity $H_c$), as well as the residual induction ($B_r$), were determined from these curves, and the results are listed in Table 5. The data revealed higher magnetic properties of the samples prepared with pH = 12.5 compared to the samples prepared with pH = 11.0. Also, the ranges of coercivity ($H_{c_B} = 1825 – ?$).
1871 Oe) and $B_r = 2308 \text{--} 2384 \text{ G}$ for the samples prepared with pH = 12.5 indicated improvement of the magnetic properties compared to BaM samples prepared by sol-gel method and sintered at similar temperatures.\textsuperscript{14}

Table 5: Magnetic parameters for the samples prepared by co-precipitation method

| pH    | Sintering Temperature | $B_r$ (G) | $H_{eb}$ (Oe) | $(BH)_{max}$ (kJ/m$^3$) |
|-------|-----------------------|-----------|---------------|-------------------------|
| 11.0  | 920 °C                | 1982      | 1628          | 6.45                    |
|       | 990 °C                | 2075      | 1709          | 6.85                    |
| 12.5  | 860 °C                | 2384      | 1871          | 8.92                    |
|       | 920 °C                | 2323      | 1844          | 8.52                    |
|       | 990 °C                | 2308      | 1825          | 8.36                    |

Fig. 5: B-H curves in the second quadrant of the hysteresis loop for all samples

Fig. 6: BH vs. $H$ curves in the second quadrant of the hysteresis loop for the samples with pH12.5 @860, and pH11@990. 1 MGOe = 7.96 kJ/m$^3$

An important figure of merit for a permanent magnetic material is the maximum energy product $(BH)_{max}$, which can be determined from the plots BH vs. H in the second quadrant of the hysteresis loop (representative curves are shown in Fig. 6). The maximum energy product (1 MGOe = 7.96 kJ/m$^3$) for all samples are shown in Table 5. The results indicated that the sample with pH =
12.5 exhibited higher maximum energy products than the samples with pH = 11.0. The data in Table 5 indicated that the sample with pH = 12.5 sintered at 860 exhibited the highest magnetic parameters. Although these parameters are not competitive with rare-earth magnets’ parameters, the alignment of the particles (by a magnetic field) can double the residual induction (considering the squareness ratio of ~ 0.5), and increase the maximum energy product by a factor of four, thus providing cost-effective magnetic materials.

**Thermomagnetic Measurements**

A powerful complementary tool for materials characterization is the measurement of the magnetization versus temperature at a constant weak applied magnetic field, to determine the magnetic phases in the sample from their respective magnetic phase transition temperatures. Fig. 7 shows the magnetization vs. temperature curves for the samples under an applied magnetic field of 100 Oe. The thermomagnetic curves revealed a single phase transition (characterized by the Curie temperature indicated by the arrows in Fig. 7) in all samples, indicating the presence of one magnetic phase. Notice that the α-Fe$_2$O$_3$ phase in the samples with pH = 11.0 does not exhibit magnetic phase transition in the range of temperature adopted in the study (as mentioned above). The Hopkinson peak just below the Curie temperature indicates the presence of small, super paramagnetic particles in the samples. The Curie temperature of (450 ± 10)°C for the samples is in agreement with ferromagnetic-to-paramagnetic transition temperature of the BaM phase (450 ºC).

**Fig. 7: Thermomagnetic curves (at an applied field of 100 Oe) for the samples**

**Conclusions**

The phase formation temperature and the purity of BaM hexaferrite in samples prepared by co-precipitation of metal and barium nitrates demonstrated sensitivity to the pH value of the stoichiometric precursor solution. All samples prepared with pH = 12.5 and sintered at temperatures from 860°C to 990°C revealed a single BaM hexaferrite phase with no secondary phases, whereas the samples with pH = 11.0 revealed the presence of a major BaM phase at sintering temperatures of 920°C to 990°C, with a minor α-Fe$_2$O$_3$ phase. The magnetic parameters of the samples with pH = 12.5 were higher than those with pH = 11.0. The results of the study indicated that improvement of the magnetic properties of BaM hexaferrite can be achieved by adopting a suitable synthesis route, and tuning the experimental conditions. The samples prepared with pH = 12.5 demonstrated improved magnetic properties suitable for permanent magnet applications. Based on the results of this study, we anticipate that the preparation of anisotropic magnets with a high degree of alignment of the easy axis of the particles prepared by this method could give magnets with high residual induction of ~ 4760 G, and maximum
energy product of ~ 35 kJ/m$^3$. These parameters are close to the theoretical values of $B_r \sim 4780$ G and $(BH)_{\text{max}} \sim 45$ kJ/m$^3$.

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**Conflict of interest**

The author declares that they have no conflict of interest.

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