Scalable solution-phase epitaxial growth of symmetry-mismatched heterostructures on two-dimensional crystal soft template

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Epitaxial heterostructures with precisely controlled composition and electronic modulation are of central importance for electronics, optoelectronics, thermoelectrics, and catalysis. In general, epitaxial material growth requires identical or nearly identical crystal structures with small misfit in lattice symmetry and parameters and is typically achieved by vapor-phase depositions in vacuum. We report a scalable solution-phase growth of symmetry-mismatched PbSe/Bi₂Se₃ epitaxial heterostructures by using two-dimensional (2D) Bi₂Se₃ nanoplates as soft templates. The dangling bond–free surface of 2D Bi₂Se₃ nanoplates guides the growth of PbSe crystal without requiring a one-to-one match in the atomic structure, which exerts minimal restriction on the epitaxial layer. With a layered structure and weak van der Waals interlayer interaction, the interface layer in the 2D Bi₂Se₃ nanoplates can deform to accommodate incoming layer, thus functioning as a soft template for symmetry-mismatched epitaxial growth of cubic PbSe crystal on rhombohedral Bi₂Se₃ nanoplates. We show that a solution chemistry approach can be readily used for the synthesis of gram-scale PbSe/Bi₂Se₃ epitaxial heterostructures, in which the square PbSe (001) layer forms on the trigonal/hexagonal (0001) plane of Bi₂Se₃ nanoplates. We further show that the resulted PbSe/Bi₂Se₃ heterostructures can be readily processed into bulk pellet with considerably suppressed thermal conductivity (0.30 W/m-K at room temperature) while retaining respectable electrical conductivity, together delivering a thermoelectric figure of merit ZT three times higher than that of the pristine Bi₂Se₃ nanoplates at 575 K. Our study demonstrates a unique epitaxy mode enabled by the 2D nanocrystal soft template via an affordable and scalable solution chemistry approach. It opens up new opportunities for the creation of diverse epitaxial heterostructures with highly disparate structures and functions.

INTRODUCTION

Epitaxy, or the growth of single-crystalline epitaxial layers, has become a major technique for the production of various device-quality semiconductor materials (1, 2) and fine-tuning the optical or catalytic properties (3–8). The growth of a thin crystalline layer on an existing single-crystalline substrate, where the atoms in the growing layer mimic the arrangement of the underlying substrate, enables higher perfection and purity as well as a better control over composition gradients than direct solidification from the melt (9). Therefore, the epitaxy approach plays a central role in the fabrication of functional electronic materials with superior performance. For example, epitaxial gallium nitride (GaN) film is grown on the sapphire substrate for the commercial white light-emitting diodes (10). It is the sole reliable method for the production of high-quality GaN thin films for bright blue light emission. Recently, the epitaxial heterostructures fabricated from two-dimensional (2D) crystals, including MoS₂/WS₂, MoS₂/MoSe₂, and WS₂/WSe₂ via the chemical vapor deposition were reported to promise a strong localized photoluminescence enhancement (11) and the application in high-voltage gain complementary inverter (12).

The first recorded successful attempt of epitaxy was reported in 1836 by Frankenheim (13), who demonstrated the now well-known case of the parallel oriented growth of sodium nitrate on calcite (calcium carbonate). The early extensive and systematic studies on a wide variety of overgrowths suggested that the identical or nearly identical crystals with small misfit in lattice parameters are essential for epitaxy. In general, the limit of lattice constant mismatch between the two materials in the heterogeneous epitaxy is generally ~5 to 10% because of the chemical bond formation, although exceptions have been demonstrated in several special cases, such as domain matching epitaxy, where integral multiples of major lattice planes match across the interface (14–16). Large lattice mismatch usually leads to excessive accumulation of strain at the interface and labilizes the obtained heterostructures (17, 18). However, there are several pioneering studies in bimetallic nanostructure synthesis, including the epitaxial growth of Ni shell on Au core despite the lattice mismatch as large as 13.6% (19–21). Alternatively, epitaxial growth between layered materials (22–27), defined as van der Waals epitaxy, continues to expand the boundary of lattice match facilitated by the effective strain relaxation resulting from the weak van der Waals interaction in the crystals. For example, layered transition metal dichalcogenide MoSe₂ was successfully grown on the cleaved mica substrate aligned along (0001) plane by molecular beam epitaxy in spite of the large lattice constant misfit up to 58% (28). However, although the lattice mismatch tolerance has been significantly promoted by various means, the requirement on the symmetry similarity between the interface planes of both crystals remains rigid in the most solution-phase
growth of nanocrystals. That is, the two crystal lattices must have an identical or nearly identical symmetry at the interface to allow epitaxial growth to occur in nanocrystals (17, 29–34). The symmetry match rule greatly limits the category of compounds that can be produced by means of epitaxy in a scalable fashion that is desirable for practical applications. A few examples with incommensurate epitaxial growth have been recently shown on mica substrate (35, 36). So far, stable solution-phase heteroepitaxial growth was limited by the symmetry/dimension compatibility, which restricts the flexibility in the design and fabrication of diverse heterostructures for practical applications.

The dangling bond–free surface in the 2D atomic crystals shows the promise for opening up a new possibility of epitaxy to bypass the symmetry match requirement (23, 25). The weak van der Waals force has been proven to exert a minimum restriction on the deposition of the crystalline layer in which epitaxial growth could happen even with an unexpectedly large lattice constant mismatch (>50%) (28). The absence of effective chemical bond formation at the interface and facile strain relaxation loosens the restriction on the structure similarity that is indispensable for the conventional epitaxy. Therefore, the clean surface in van der Waals crystal could be further expected to break the symmetry match rule by manipulating the interaction between the substrate and the growth layer.

Here, we report a solution-phase symmetry-mismatched epitaxial growth of cubic PbSe crystal (Fm$ar{3}$m) on rhombohedral Bi$_2$Se$_3$ 2D nanoplate (R$ar{3}$m) in which the square PbSe (001) layer forms on the trigonal/hexagonal (0001) plane of Bi$_2$Se$_3$ nanoplates. The (001) plane of face-centered cubic (fcc) PbSe crystal exhibits a typical fourfold symmetry, whereas that of the rhombohedral Bi$_2$Se$_3$ occupies a threefold atom arrangement. Each atomic layer within the quintuple layer has a sixfold rotational axis, although the rhombohedral Bi$_2$Se$_3$ crystal (R$ar{3}$m) does not really have one. For simplicity, hereafter, we designate Bi$_2$Se$_3$ (0001) layer as having a sixfold symmetry. However, we also note that the symmetry of the 3D crystal is distinct from that of the individual crystal plane, and thus, they are expressed in different terms for better illustration (Hermann-Mauguin notation is used for the bulk crystal, and the rotational axis of individual atomic layer is mainly discussed). Despite the distinct lattice geometry, PbSe (001) grows on Bi$_2$Se$_3$ (0001) uniformly with a moiré pattern of sixfold symmetry. The 2D Bi$_2$Se$_3$ nanoplate functions as a “soft” template in which the interface Bi$_2$Se$_3$ layer expands to accommodate the PbSe lattice, whereas the rest of the layers remain intact so that the internal strain in the heterostructure is minimized. Benefiting from the dangling bond–free, clean surface of the 2D Bi$_2$Se$_3$ nanoplates, the rule of symmetry match could be relaxed in the epitaxial growth of solution-phase nanocrystals. To further understand the mechanism of the unique epitaxial relationship, we adopted a density functional theory (DFT) calculation to simulate several possible relative orientations between the two crystals. The calculation results suggest the lowest interfacial energy for the PbSe (001)/Bi$_2$Se$_3$ (0001) structure, which is consistent with the observed experimental result. With nearly perfect epitaxial interfaces, the obtained heterostructures exhibit a reduced thermal conductivity (~0.30 W/mK at room temperature) without significantly sacrificing the electronic properties and thus enable an improved thermoelectric performance, opening an affordable and scalable approach to bulk quantities of epitaxial nanostructures with precisely engineered electronic, optoelectronic, thermal, and thermoelectric properties.

RESULTS
Layered Bi$_2$Se$_3$ nanoplates were produced following our previously reported polyol method (37), which served as the substrate for the epitaxial growth of the cubic PbSe crystal. After the formation of Bi$_2$Se$_3$ nanoplates in the solution, Pb and Se precursors were slowly injected into the flask to allow the initial and continued growth of PbSe under a relatively mild condition. A schematic illustration for the epitaxial growth of the cubic PbSe crystal on the rhombohedral Bi$_2$Se$_3$ nanoplate is shown in Fig. 1.

The powder x-ray diffraction (PXRD) pattern of the as-synthesized sample can be indexed as two crystal phases, including the rhombohedral Bi$_2$Se$_3$ [R$ar{3}$m; Joint Committee on Powder Diffraction Standard (JCPDS) card no. 00-033-0214] and cubic PbSe (Fm$ar{3}$m; JCPDS card no. 03-065-0300) (fig. S1). The morphology and structure of the as-synthesized heterostructure were further characterized with transmission electron microscopy (TEM). Figure 2A presents a typical TEM image of the heterostructure in which the PbSe layer partially covers the surface of the Bi$_2$Se$_3$ nanoplate. The boundary between the pure Bi$_2$Se$_3$ and PbSe/Bi$_2$Se$_3$ regions was labeled with a blue dashed line. A uniform moiré pattern with an approximate hexagonal symmetry is clearly observed in the area with the deposition of the PbSe layer on Bi$_2$Se$_3$ (fig. 2, A and B). The high-resolution TEM (HRTEM) image shows clearly resolved lattice fringes that are dominated by the hexagonal Bi$_2$Se$_3$ crystal lattice (Fig. 2B). In contrast, no similar pattern was observed in the area without PbSe (fig. S2, A and B). The moiré pattern was also identified in the scanning TEM (STEM) image (figs. S3 and S4).

The selected-area electron diffraction (SAED) patterns unraveled the relative crystallographic orientation of the PbSe layer and Bi$_2$Se$_3$ crystals in the heterostructure. SAED patterns on the region with moiré pattern (Fig. 2B) give two sets of diffraction spots with a hexagonal and a square symmetry, respectively (Fig. 2C). Each diffraction spot in the hexagonal pattern corresponds to the (11-20) family plane of the Bi$_2$Se$_3$ nanoplate (fig. S2C), and each diffraction spot in the square pattern can be indexed to the (110) family plane of the cubic PbSe layer. On the basis of the electron diffraction analysis, the crystal structure of PbSe and Bi$_2$Se$_3$ as well as the relative orientation are illustrated in Fig. 2 (D and E). Again, the single Bi$_2$Se$_3$ quintuple layer is considered as sixfold symmetric rather than threefold for simplification. The [11-20] direction of Bi$_2$Se$_3$ aligned well with the [110] direction of PbSe with essentially overlapping diffraction spots, suggesting an epitaxial relationship. The interplane distances of PbSe (110) and Bi$_2$Se$_3$ (11-20) planes are 4.29 and 4.14 Å, respectively, which are close enough (3.5% mismatch) for the epitaxial growth to occur. Therefore, the PbSe layer that deposited on the Bi$_2$Se$_3$ nanoplates with (001)/(0001) plane paralleled to each other and [110]/[11-20] axis aligned (Fig. 2F) was unequivocally determined.

DISCUSSION
Typical moiré patterns observed in TEM image originated from the mismatch between two distinct periodic lattices (38–42). However, overlapping the (001) plane of PbSe with the (0001) plane of Bi$_2$Se$_3$ could not produce the sixfold symmetric moiré pattern observed in our experiments (Fig. 2A). As a result, an additional lattice needs to be present in the heterostructure to produce the sixfold moiré pattern. The higher-order diffraction spots for Bi$_2$Se$_3$ on the heterostructure suggest the existence of an expanded Bi$_2$Se$_3$ lattice besides the
pristine one. In the higher-order diffraction spots, each of the hexagonal spots splits into two (Fig. 2H). The brighter diffraction spots match well with the (11-20) lattice spacing of pristine Bi$_2$Se$_3$ crystal (Fig. 2G). In contrast, the weaker spots indicate an expanded Bi$_2$Se$_3$ lattice by about 3.5% (from 4.14 to 4.29 Å). The spacing of the enlarged Bi$_2$Se$_3$ (11-20) plane, 4.29 Å, coincides with the lattice spacing of (110) planes in PbSe crystal. Consequently, the expansion in the Bi$_2$Se$_3$ layers is attributed to the lattice constant mismatch in the [110] direction along which PbSe and Bi$_2$Se$_3$ crystals align with each other. The Bi$_2$Se$_3$ layers at the interface are thus expanded to accommodate the larger PbSe lattice.

The deformation of the existing lattice in underlying substrate, instead of the incoming epitaxial layers, to ensure a lattice match is distinct from most of the conventional epitaxy. Here, the layered nature and weak van der Waals interlayer interaction play a key role in the special expansion of the atomic layer on the underlying Bi$_2$Se$_3$ substrate and make it a unique soft template. Between each quintuple layer in the Bi$_2$Se$_3$ crystal, only the weak van der Waals force is present to hold the crystal together, which is considered to be much weaker than the typical chemical bonds. During the expansion or contraction of one layer of atoms, the adjacent quintuple layers are not strongly coupled to match the deformation that is typical in conventional epitaxy (25). The soft nature of the 2D Bi$_2$Se$_3$ crystal renders the opportunity that only the first interface layer of the atomic crystals expands (fig. S5) to accommodate the larger PbSe lattice, whereas the rest of the layers remain intact.

Compared with the deformation of the 3D PbSe crystal, the expansion of 2D Bi$_2$Se$_3$ layers at the interface introduces weaker overall strain in the heterostructure, which is thermodynamically preferred. Furthermore, the elastic constants of deformation within the (001) plane of Bi$_2$Se$_3$ and PbSe are 103.2 and 120.8 GPa (43, 44), respectively. Therefore, in the perspective of stiffness, Bi$_2$Se$_3$ is more likely to deform compared with PbSe under the same strain that exists at the interface. To confirm the proposed atomic model, we simulated the moiré pattern by combining the pristine (0001) plane of Bi$_2$Se$_3$ (4.14 Å) with an expanded lattice (4.29 Å) (fig. S5). Expectedly, the resulted moiré pattern exhibits a sixfold symmetry (Fig. 2I) that is highly consistent with the experimentally observed moiré pattern in our heterostructure (Fig. 2, A and B).

We have further conducted the cross-sectional TEM (Fig. 3A) and STEM (Fig. 3B) studies to further confirm the atomic structure of the PbSe/Bi$_2$Se$_3$ epitaxial heterostructure. The composition line scan profile across the interface obtained shows that Pb and Bi contents are solely present in PbSe and Bi$_2$Se$_3$ regions, respectively, whereas Se exists in both materials (Fig. 3C). Because Se density in Bi$_2$Se$_3$ (2.47 g/cm$^3$) is higher than that in PbSe (2.24 g/cm$^3$), the Se amount increases slightly from PbSe to Bi$_2$Se$_3$ crystal. 2D mapping of Pb, Bi, and Se element (Fig. 3D) further provides an explicit distribution of each element. In both line scan profile and elemental mapping, the HRTEM of the interface (Fig. 3E) indicates that both segments exhibit excellent crystallinity with an atomically sharp interface. The clear fringe in the PbSe showed a period of
0.31 nm, as expected for the fcc PbSe (001) plane. The line scan profile and elemental mapping of Bi and Pb show a gradual transition across the interface, which might be due to the resolution of the STEM image. Together, the cross-sectional TEM studies further confirm the epitaxial growth of highly crystalline PbSe layer on top of the Bi2Se3 nanoplate, as illustrated by the schematic in Fig. 3F.

The symmetry-mismatched epitaxy observed in the PbSe/Bi2Se3 system is a special crystal growth in solution-phase synthesized nanocrystals (36). The atoms in the (001) plane of the fcc PbSe crystal exhibit a square symmetry, whereas the (0001) plane of the rhombohedral Bi2Se3 has a trigonal/hexagonal lattice (for single atomic layer). Here, we discuss the symmetry of individual atomic layer instead of the 3D crystal. To date, most of the epitaxial growth reported in the solution phase rigidly follow the rule of lattice symmetry matching requirement, including the typical cases of fourfold fcc Pd (100)//fcc Pt (100) (45), sixfold fcc Pt (111)//hexagonal MoS2 (001) (46), and sixfold wurtzite CdS (001)//wurtzite CdSe (001) (47). The alike symmetry between the crystals or the specific growth planes is mandatory to saturate the dangling bonds that are present at the interface. However, the dangling bond–free surface in the 2D atomic crystals promises a totally new possibility of epitaxial growth. The cleavage of the 2D layered compounds, such as Bi2Se3 and MoS2, could create a clean surface that is free of unsaturated atoms. The weak van der Waals force applies a weaker regulation than the unsaturated chemical atoms on the surface of typical crystalline layer, as demonstrated by several successful epitaxial growths with large lattice misfit (up to >50%) (22, 24, 25, 28, 35). In this case, the layered Bi2Se3 nanoplate guides the growth of the PbSe layer but does not require an exactly conformal lattice with one-to-one bond matching. The soft nature of the layered Bi2Se3 allows the deformation of the atomic layers near the interface without causing severe distortion of the entire nanoplates. The interface Bi2Se3 layers expand to match the larger PbSe lattice (by 3.5%) and ensure the energy minimum epitaxial growth that could not be realized in the traditional rigid substrates. Accordingly, the layered crystals that are held together by the loose van der Waals force are demonstrated to function as the unique soft substrate for the epitaxial growth of highly dissimilar materials. The
discovery of the new epitaxy mode would open up new possibilities to enable the atomic-scale integration of materials with highly disparate crystal structures and functions.

Considering the similar sixfold symmetry of (0001) surface of the underlying Bi\textsubscript{2}Se\textsubscript{3} and (111) surface of the cubic PbSe, a symmetry-matched epitaxial relationship of PbSe (111)//Bi\textsubscript{2}Se\textsubscript{3} (0001) would have been a logical expectation instead of our observed symmetry-mismatched PbSe (001)//Bi\textsubscript{2}Se\textsubscript{3} (0001). To better understand the unique symmetry-mismatched epitaxy, we have constructed a series of atomic models for PbSe/Bi\textsubscript{2}Se\textsubscript{3} heterostructures and conducted DFT calculations to probe the interfacial bonding and energy. In particular, three types of PbSe planes, including (001), (011), and (111) were considered for epitaxial interfacing with the Bi\textsubscript{2}Se\textsubscript{3} (0001) surface (Fig. 4), and the corresponding interfacial energy was calculated. Significantly, the DFT calculation indicates that PbSe (001)//Bi\textsubscript{2}Se\textsubscript{3} (0001) is the most preferred epitaxial relation with the lowest interfacial energy of 0.031 eV/Å\textsuperscript{2}, followed by interfacial energy of 0.046 eV/Å\textsuperscript{2} in PbSe (111)//Bi\textsubscript{2}Se\textsubscript{3} (0001) and then 0.056 eV/Å\textsuperscript{2} in PbSe (011)//Bi\textsubscript{2}Se\textsubscript{3} (0001) (Fig. 4). In addition, the smallest equilibrium atom distances in PbSe (001)//Bi\textsubscript{2}Se\textsubscript{3} (0001) and PbSe (011)//Bi\textsubscript{2}Se\textsubscript{3} (0001) are 3.30 and 3.27 Å, respectively, comparable to the typical Pb–Se bond distance, suggesting the effective bond formation between PbSe (001) and (011) plane with Bi\textsubscript{2}Se\textsubscript{3} (0001) plane. It is worth noting that the interfacial Pb–Se distance (3.30 Å) is smaller than the distance of selenium atoms between two van der Waals layers (3.49 Å), indicating that the top Bi\textsubscript{2}Se\textsubscript{3} layer has a strong coupling to the epitaxial PbSe layer. In contrast, the smallest equilibrium atom distance in the PbSe (111)//Bi\textsubscript{2}Se\textsubscript{3} (0001) interface is 3.59 Å, which is too large for effective bond formation. Therefore, no chemical bond is expected to be present in this model, further confirming that the PbSe (111)//Bi\textsubscript{2}Se\textsubscript{3} (0001) epitaxial relationship is unfavorable, in spite of a similar sixfold symmetry (Fig. 4C). Another factor that influences the epitaxy selectivity is the dangling bond density at the interface. On the basis of the simulated bonding configuration (Fig. 4), the dangling bond densities for PbSe (001), (011), and (111) surfaces on the Bi\textsubscript{2}Se\textsubscript{3} (0001) surface are 0.093/Å\textsuperscript{2}, 0.113/Å\textsuperscript{2}, and 0.185/Å\textsuperscript{2}, respectively. PbSe (001) exhibits the lowest dangling bond density, further suggesting that PbSe (001)//Bi\textsubscript{2}Se\textsubscript{3} (0001) is the preferred epitaxial relationship. Considering all the above factors, the PbSe (111)//Bi\textsubscript{2}Se\textsubscript{3} (0001) model exhibits the largest number of nonbonded electrons, which induces a great lability in the structure. In contrast, the PbSe (001)//Bi\textsubscript{2}Se\textsubscript{3} (0001) model shows improved stability with fewer dangling bonds. Together, the DFT calculation results support our interpretation of the experimentally observed epitaxial relationship in the PbSe/Bi\textsubscript{2}Se\textsubscript{3} heterostructure.

The formation of the heterointerface in the nearly perfect epitaxial heterostructures could suppress the thermal transport while largely retaining the electronic properties, which is desirable for thermoelectric applications. In particular, previous studies have shown that the lamellar nanostructures or superlattices could enable significant thermal conductivity reduction and thermoelectric enhancement (48–50). The assembled PbSe/Bi\textsubscript{2}Se\textsubscript{3} heterostructures exhibit superlattice-like structure in the local region and therefore may offer unique opportunities in thermoelectric devices. To explore the thermoelectric properties of the high-quality PbSe/Bi\textsubscript{2}Se\textsubscript{3} heterostructures, we processed the nanostructured powders into bulk pellet using hot pressing to enable thermoelectric property measurement. At room temperature, both the values of electrical conductivity and Seebeck coefficient of PbSe/Bi\textsubscript{2}Se\textsubscript{3} heterostructure are lower than those of the pristine Bi\textsubscript{2}Se\textsubscript{3} nanoplate, which leads to a smaller power factor (Fig. 5, A to C). Notably, with increasing temperature, the power factor of PbSe/Bi\textsubscript{2}Se\textsubscript{3} rises rapidly and
becomes about 70% higher than that of pristine Bi$_2$Se$_3$ at 575 K because of the simultaneous increase in both electrical conductivity and Seebeck coefficient (Fig. 5C). The most interesting property of the heterostructure is the extremely low thermal conductivity within the measured temperature range (Fig. 5, D and E). At the temperature between 298 and 575 K, the thermal conductivity of the PbSe/Bi$_2$Se$_3$ pellet ranges from 0.30 to 0.29 W/m·K, which is considerably lower than that of the Bi$_2$Se$_3$ nanoplate pellet (0.57 to 0.50 W/m·K) and PbSe (0.9 to 1.4 W/m·K) (51, 52). The efficient phonon scattering at the PbSe and Bi$_2$Se$_3$ heterointerface is considered to be mainly responsible for such a low thermal conductivity (49, 53–55), which is similar to the mechanism in PbTe and Bi$_2$Te$_3$ nanowire heterostructure (56). On the basis of the measured electrical conductivities, Seebeck coefficients, and thermal conductivities, we have

### Table 1

| Interfacial Slabs  | (001)     | (011)     | (111)     |
|--------------------|-----------|-----------|-----------|
| Interfacial Energy (eV/Å$^2$) | 0.031     | 0.046     | 0.056     |
| Interfacial Bond Length (Å)      | 3.30      | 3.27      | 3.59      |
| Dangling Bond Density (1/Å$^2$)  | 0.093     | 0.113     | 0.185     |

**Fig. 4.** DFT calculation of heterostructure models with various orientations. (A to C) Atomic structure with Bi$_2$Se$_3$ (0001) parallel to PbSe (001) (A), (011) (B), and (111) (C) after energy relaxation. Table shows the interfacial energy, bond length, and dangling bond density for each type of interface.

### Fig. 5

**Thermoelectric performance of pristine Bi$_2$Se$_3$ nanoplate and the heterostructure.** (A to F) The electrical conductivity $\sigma$ (A), Seebeck coefficient $S$ (B), power factor $\sigma S^2$ (C), thermal diffusivity $\alpha$ (D), thermal conductivity $\kappa$ (E), and figure of merit $ZT$ (F) of pristine Bi$_2$Se$_3$ nanoplate and PbSe/Bi$_2$Se$_3$ heterostructure bulk, which were prepared by hot pressing under the same conditions.
calculated the temperature-dependent thermoelectric figure of merit ($ZT = S^2\sigma/k$) of both nanostructured pellets (Fig. 5F). Significantly, the PbSe/Bi$_2$Se$_3$ heterostructures exhibit considerably higher $ZT$ value than the pure Bi$_2$Se$_3$ with a three-time enhancement at 575 K, which can be largely attributed to the ultralow thermal conductivity and increased Seebeck coefficient of the epitaxial heterostructures. Together, the PbSe/Bi$_2$Se$_3$ epitaxial heterostructure could successfully suppress the thermal transport without seriously sacrificing the electrical conductivity via enhanced phonon scattering and increase the Seebeck coefficient, thus leading to significantly improved thermoelectric performance.

In summary, we have reported an example of symmetry-mismatched epitaxial growth of the PbSe (001) plane on the 2D Bi$_2$Se$_3$ nanoplate (0001) plane in the solution phase. The dangling bond-free (0001) plane of Bi$_2$Se$_3$ exerts a weak regulation on the growth of the PbSe layer because of the absence of one-to-one atomic chemical bond formation and results in a unique soft template for epitaxy. The DFT calculations suggest the lower interfacial energy in the PbSe (001)//Bi$_2$Se$_3$ (0001) model than in the PbSe (011)//Bi$_2$Se$_3$ (0001) or PbSe (111)//Bi$_2$Se$_3$ (0001) model and thus a more thermodynamically stable structure. Our study on the symmetry-mismatched epitaxial growth in liquid-phase nanomaterials enriches the toolbox for the fabrication of high-quality heterostructures via the epitaxy method and opens up new possibilities in engineering the interface within composite materials to enable high-performance electronic, optoelectronic, and thermoelectric devices. In particular, the growth of PbSe/Bi$_2$Se$_3$ heterostructures or superlattices could effectively reduce the thermal conductivity by the interface scattering of phonon and therefore provides a scalable approach to bulk quantities of epitaxial nanostructures with precisely engineered thermoelectric properties.

**MATERIALS AND METHODS**

**Synthesis of lead selenide/bismuth selenide heterostructure**

For the bismuth selenide nanobranches, 0.2 mmol of Bi(NO$_3$)$_3$·5H$_2$O (0.0970 g), 0.3 mmol of NaSeO$_3$ (0.0519 g), and 2 mmol of polyvinylpyrrolidone (0.2223 g) were dissolved in 10 ml of ethylene glycol (EG). The mixture was stirred for 10 min and then heated to 190°C (in about 12 min) in a 25-ml three-neck flask equipped with a thermal couple and a reflux condenser in a heating mantle. After 3 h, the temperature was decreased to 180°C and allowed to stabilize for 20 min. One milliliter of 0.1 M Pb(CH$_3$COO)$_2$·3H$_2$O and 1 ml of 0.1 M Na$_2$SeO$_3$ both in EG solution were simultaneously injected into the flask using a syringe pump with a rate of 250 μl/min. After the temperature was maintained at 180°C for 3 h, the heating mantle was removed and the mixture was allowed to cool down to room temperature naturally. The mixture was then centrifuged at 12,000 rpm for 10 min after the addition of 30 ml of isopropanol. The supernatant was discarded, and the solid was dispersed in another 40 ml of isopropanol. The solid was washed with isopropanol and centrifuged three times before the final product was dispersed in isopropanol for further characterization.

**DFT modeling**

The Vienna Ab initio Simulation Package (VASP) with the projector-augmented wave method using the Perdew–Becke–Ernzerhof generalized gradient approximation for the exchange-correlation functional was used to perform structural optimization and electronic structure calculation. A plane-wave basis with a cutoff energy of 450 eV and Γ-centered k-point meshes of constant density was used to fully relax both bulk and slab structures with an energy convergence threshold of 10$^{-5}$ eV and residual forces of less than 10$^{-2}$ eV/Å. For example, Γ-centered k-point meshes of 16 × 16 × 1 were used for a single quintuple layer of Bi$_2$Se$_3$.

**Thermoelectric measurement**

To characterize the thermoelectric properties in out-of-plane direction, disc [12.7 mm (D) × 2 mm (H)] and cylinder [4 mm (D) × 10 mm (H)] specimens were separately prepared for thermal conductivity and power factor measurement. For disc specimens, the dried powders were ground and loaded into a graphite die with an inner diameter of 12.7 mm (for cylinder samples, the inner diameter of the die was 4 mm) in the glove box under an argon atmosphere with an oxygen level below 3.5 parts per million. Then, the graphite die with loaded powder was removed from the glove box and immediately sintered by dc-induced hot pressing at 663 K for 15 min at a force of 1.4 metric tons (for cylinder samples, the force is ~0.1 metric ton to ensure a similar pressure). The hot-pressed discs had a thickness of about 2 mm, and the cylinder specimens had a length of around 10 mm.

The hot-pressed discs were used for out-of-plane thermal conductivity characterizations, whereas the cylinder specimens were used directly for the measurement of out-of-plane electrical properties. The electrical conductivity of the samples was measured by a four-point dc switching technique, and the Seebeck coefficient was measured by a static dc method on the basis of the slope of the voltage versus temperature difference curves using the commercial equipment (ZEM-3, ULVAC Riko) under helium atmosphere. The out-of-plane thermal conductivity was measured on the disc specimens. Thermal conductivity $\kappa = dDC_p$ was calculated using the measured density ($d$) by Archimedean method, specific heat ($C_p$) by differential scanning calorimetry (DSC 404 C, Netzsch), and thermal diffusivity ($D$) by the laser flash method (LAF 447 Nanoflash, Netzsch). The errors of measurement for electrical resistivity, Seebeck coefficient, and thermal conductivity were ±5, ±5, and ±7%, respectively. Here, all the reported values were measured and compared in out-of-plane direction of Bi$_2$Se$_3$ and PbSe/Bi$_2$Se$_3$ samples.

**Characterization**

Characterizations were carried out using HRTEM, SAED, HAADF-STEM–EDS (TEM, T12 Quick CryoEM, and CryoET FEI; acceleration voltage, 120 kV; Titan S/TEM FEI; acceleration voltage, 300 kV), and PXRD (PAAnalytical X’Pert Pro x-ray powder diffractometer). The cross-sectional sample was prepared by covering the film sample on the SiO$_2$/Si substrate with a layer of polycrystalline Pt and then cleaving with FIB.

**SUPPLEMENTARY MATERIALS**

Supplementary material for this article is available at http://advances.sciencemag.org/cgi/content/full/2/10/e1600993/DC1

fig. S1. PXRD pattern for the PbSe/Bi$_2$Se$_3$ heterostructure.

fig. S2. HRTEM analysis of the pure Bi$_2$Se$_3$ region in the PbSe/Bi$_2$Se$_3$ heterostructure.

fig. S3. Low-magnification representative STEM image of the PbSe/Bi$_2$Se$_3$ heterostructure.

fig. S4. High-magnification representative STEM image of the PbSe/Bi$_2$Se$_3$ heterostructure.

fig. S5. Atomic crystal structure for the intrinsic and expanded Bi$_2$Se$_3$ (0001) layers.

note S1. DFT modeling of PbSe (001)–Bi$_2$Se$_3$ (0001), PbSe (011)–Bi$_2$Se$_3$ (0001), and PbSe (111)–Bi$_2$Se$_3$ (0001) interfaces.
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