Small scale rotational disorder observed in epitaxial
graphene on SiC(0001)

Andrew L Walter\textsuperscript{1,2,3,8}, Aaron Bostwick\textsuperscript{1}, Florian Speck\textsuperscript{4}, Markus Ostler\textsuperscript{4}, Keun Su Kim\textsuperscript{1}, Young Jun Chang\textsuperscript{5}, Luca Moreschini\textsuperscript{1}, Davide Innocenti\textsuperscript{6}, Thomas Seyller\textsuperscript{7}, Karsten Horn\textsuperscript{2} and Eli Rotenberg\textsuperscript{1}

\textsuperscript{1} Advanced Light Source (ALS), E O Lawrence Berkeley National Laboratory, Berkeley, CA 94720, USA
\textsuperscript{2} Department of Physical Chemistry, Fritz-Haber-Institut der Max-Planck-Gesellschaft, Faradayweg 4-6, D-14195 Berlin, Germany
\textsuperscript{3} Donostia International Physics Centre, Paseo Manuel de Lardizabal, 4, 20018 Donostia-San Sebastian, Spain
\textsuperscript{4} Lehrstuhl für Technische Physik, Universität Erlangen-Nürnberg, Erwin-Rommel-Strasse 1, D-91058 Erlangen, Germany
\textsuperscript{5} Department of Physics, University of Seoul, Seoul, 130-743, Korea
\textsuperscript{6} University of Rome (Tor Vergata), Rome I-00173, Italy
\textsuperscript{7} Institut für Physik, Technische Universität Chemnitz, Reichenhainer Straße 70, 09126 Chemnitz, Germany

E-mail: andrew_walter@ehu.es

New Journal of Physics 15 (2013) 023019 (8pp)
Received 21 September 2012
Published 11 February 2013
Online at http://www.njp.org/
doi:10.1088/1367-2630/15/2/023019

Abstract. Interest in the use of graphene in electronic devices has motivated an explosion in the study of this remarkable material. The simple, linear, Dirac cone band structure offers a unique possibility to investigate its finer details by angle-resolved photoelectron spectroscopy (ARPES). Indeed, ARPES has been performed on graphene grown on metal substrates but electronic applications require an insulating substrate. Epitaxial graphene grown by the thermal decomposition of silicon carbide (SiC) is an ideal candidate for this
due to the large scale, uniform, graphene layers produced. The experimental spectral function of epitaxial graphene on SiC has been extensively studied. However, until now the cause of an anisotropy in the spectral width of the Fermi surface has not been determined. In the current work we show, by comparison of the spectral function to a semi-empirical model, that the anisotropy is due to small scale rotational disorder (\( \sim \pm 0.15^\circ \)) of graphene domains in graphene grown on SiC(0001) samples. The complicated shape described by the line-width is accurately reproduced by the semi-empirical model only when rotational disorder is included. While spectra from rare regions of the sample containing only one or two rotational domains is also presented. In addition to the direct benefit in the understanding of graphene’s electronic structure this work suggests a mechanism to explain similar variations in related ARPES data.

Interest in the single layer of hexagonally coordinated carbon atoms, known as graphene, has been intense ever since the discovery of its unusual electronic properties [1]. An understanding of the electronic properties is essential if graphene applications are to be realized. Angle resolved photoemission spectroscopy (ARPES) measurements provide the most direct method to investigate the electronic band structure. This technique requires large well defined samples, which can only be realized by producing graphene on a crystal substrate. ARPES has been performed on graphene on metal substrates, however electronic applications will require insulating or semiconducting substrates. A significant number of ARPES studies have therefore been performed on graphene grown epitaxially on silicon carbide (SiC) by thermal decomposition [2, 3]. This preparation method is a very promising candidate for applications because the production process can be scaled up, uses common semiconductor processing steps, and provides large scale uniform layers.

This material can be considered an important testbed for exciting solid state physics and interest has turned to the fine details of its band structure, as observed by ARPES. In this context we compare ARPES measurements to a semi-empirical photoemission model. Comparison of the model to experimental data accounted for almost all features of the electronic structure, with the exception of an anisotropy in the spectral width when sampling the band structure along different directions in reciprocal space. We show that this anisotropy is explained by a \( a \pm 0.15^\circ \) rotational disorder of the graphene domains. Figure 1(a) shows an example of the well known experimental spectral function obtained from epitaxial graphene on SiC(0001). This shows that the graphene is n-doped, i.e. the Dirac energy \( (E_D) \), or linear band crossing point, is shifted to \( \sim -0.5 \text{ eV} \). For graphene grown in this method it has been demonstrated to be separated from the substrate by the so-called buffer layer with \((6\sqrt{3} \times 6\sqrt{3})R30^\circ \) periodicity (hence forth \( 6\sqrt{3} \)) [4]. The anisotropy in the Fermi surface intensity (decrease in intensity in one direction) [5], the increase in the intensity between the Fermi surface (0 eV constant energy slice) and \( \sim 200 \text{ meV} \) [6] and the offset of the bands above and below the Dirac crossing, \( E_D \), [7–9] have all been successfully described. Until now the anisotropy in the spectral width of the Fermi surface has not been explained. This anisotropy is seen in figure 1(a)(i) as an increased width in the vertical, \( k_y \) (\( \overline{KK} \)), direction when compared to that in the horizontal, \( k_x \) (\( \overline{KK} \)), direction. This variation is not confined to the Fermi surface, but appears across all energies.
This line width variation is important for a detailed analysis of the spectral function in many contexts such as gap formation, the examination of many-body interactions and the investigation of the Berry’s phase in graphene. The current work provides a simple explanation of this feature, in terms of small scale rotational disorder, which is essential to the discussion of the electronic structure of graphene. In fact many papers have used intensity and line-width variations in ARPES data to discuss the existence of various quasiparticles \([9–15]\) and in discussions of the Berry’s phase \([11, 16, 17]\) in graphene. The current work therefore provides an invaluable insight into ARPES spectral variations and in the understanding of these more exotic features.

ARPES were obtained at the Maestro end station (SES-R4000 analyzer) at beamline 7 of the Advanced Light Source, Lawrence Berkeley National Laboratory. Spectra were taken at \(\sim 20\) K, at \(< 2 \times 10^{-10}\) Torr using 95 eV photons giving an overall resolution of \(\sim 25\) meV and \(0.01\) Å\(^{-1}\). Epitaxial graphene on SiC(0001) was prepared either by annealing in ultra-high vacuum \([2]\) (vacuum grown) or by annealing in Ar \([3]\) (argon grown) using a custom built reactor \([18]\). The decomposition of SiC in Ar leads to an improved crystalline quality \([3]\).

In order to generate a semi-empirical model of the experimental ARPES data (spectral function) the simplest approach is to start with an unbroadened \(E(k)\) dispersion relation, a so-called bare band. The bare band used in the semi-empirical ARPES model is a first nearest neighbor tight binding model fit to experimental graphene on \(6\sqrt{3}\) data. This models the \(\pi\) bands via the relations

\[
E_{\text{bare}}(k) = \frac{\epsilon_{2p} \pm \gamma_0 \omega(k)}{1 \pm s_0 \omega(k)},
\]

\[
\omega(k) = \sqrt{1 + 4 \cos^2 \left(\frac{\sqrt{3} a k_y}{2}\right) \cos \left(\frac{a k_x}{2}\right) + 4 \cos^2 \left(\frac{a k_x}{2}\right)}
\]

with a lattice constant, \(a = 2.46\) Å. The fitted parameters, \(\gamma_0 = -3.24\) eV and \(s_0 = 0.0425\) eV, are those found by Bostwick \textit{et al} \([17]\). The final fitted parameter, \(\epsilon_{2p}\), is the offset of the Dirac energy, \(E_D\), from the Fermi level due to doping of the graphene by the substrate and is determined by comparison to the ARPES measurements. This approach has been shown
Figure 2. Diagram showing the (a) Brillouin zone boundaries for graphene with the first, second, third and fourth Brillouin zone $K$ point radial lines (dashed, blue, lines) of graphene, (b) schematic of a selected $K$ point showing the effect of small scale rotational disorder and (c) selected experimental (dashed lines) and semi-empirical model (solid lines) intensity profiles in the $\overline{KK}$ and $\Gamma K$ directions. In (a) the Fermi surfaces indicate the $K$ points at which measurements were undertaken.

previously [17] to accurately model the bare band dispersion within the region considered in the present paper (within 1 eV of the Fermi level). Broadening of the bare band is then introduced to the model through the spectral function relation [19]

$$A(E, \mathbf{k}) = \frac{|\text{Im}\Sigma(E, \mathbf{k})|}{(E - E_{\text{bare}}(\mathbf{k}) - \text{Re}\Sigma(E, \mathbf{k}))^2 + |\text{Im}\Sigma(E, \mathbf{k})|^2}. \quad (3)$$

The self energy is determined using the semi-empirical method of Bostwick et al [20], where the linewidth of the ARPES momentum density curves (MDCs) are used to determine the imaginary component of the self energy, which is Hilbert transformed to get the real component. This experimental self energy is then used to recreate the experimental data and a self-consistent fitting used to further refine the self energy. An additional Gaussian broadening term is added to the current model to account for experimental broadening, $dE = 25 \text{ meV}$.

Rotational disorder of graphene on metal substrates such as Cu(111) [21] and Pt(111) [22] has been shown to lead to significant anisotropic spectral broadening. Therefore we attempted to model the much smaller anisotropic broadening seen in graphene on SiC with a similar small rotational disorder. To model the effect of rotational disorder several three-dimensional spectral functions, rotated around the $\Gamma$ point by small angles, are summed together. This is illustrated, for a two-dimensional Fermi surface (0 eV slice through momentum space), in figure 2(b). The non-rotated Fermi surface is the solid arc around the $K$ point, two further Fermi surfaces (dashed arcs) are shown rotated by a small amount around $\Gamma$. The effect on the Fermi surface is that it
Figure 3. Fitted Fermi surface data for vacuum grown (solid light, orange, lines), argon grown (solid dark, green, lines) and semi-empirical model (dashed, blue, lines) for the three first Brillouin $K$ points indicated in figure 2. Position (i), amplitude (ii) and Gaussian linewidths (iii) obtained from Lorentzian–Gaussian fits to the Fermi surface are presented. In all cases the Lorentzian width is set to $0.15 \, \text{Å}^{-1}$ ensuring that the Gaussian width describes the variation in the width of the Fermi surface.

appears broader in the $\overline{KK}$ direction than in the $\overline{\Gamma K}$ direction. Examples of the Fermi surface intensity profiles in the $\overline{KK}$ and $\overline{\Gamma K}$ directions for three different regions on a sample are shown in figure 2(c). Fitted Fermi surface data presented in figures 3 and 4 are obtained by taking similar intensity line profiles of the Fermi surface in $1^\circ$ steps around the $K$ point with the $\overline{\Gamma K}$ direction being set as the zero angle. The Lorentzian width is set to the width of the Fermi surface in the $\overline{\Gamma K}$ direction ($0.15 \, \text{Å}^{-1}$), ensuring the Gaussian line width describes the variation in width of the Fermi surface.

In order to investigate the anisotropy in the width of the Fermi surface, experimental spectral functions at a number of $K$ points in the graphene Brillouin zone (an example spectral function is shown in figure 2(a)) were obtained. The $K$ points are all equivalent with respect to the proposed rotational disorder. This is not the case for the higher order Brillouin zones (BZ2, BZ3 and BZ4 in figure 2) where the axis of rotation no longer lies in the $\overline{\Gamma K}$ direction. Investigation of the higher Brillouin zone experimental spectral functions provides an important test of the rotational disorder model, as discussed in more detail below. Fitted Fermi surface data

New Journal of Physics 15 (2013) 023019 (http://www.njp.org/)
Figure 4. Fitted Fermi surface data for vacuum grown (solid light, orange, lines), argon grown (solid dark, green, lines) and semi-empirical model (dashed, blue, lines) for the higher order Brillouin zone $K$ points indicated in figure 2. Position (i), amplitude (ii) and Gaussian linewidths (iii) obtained from Lorentzian–Gaussian fits to the Fermi surface are presented. In all cases the Lorentzian width is set to $0.15\,\text{Å}^{-1}$ ensuring that the Gaussian width describes the variation in the width of the Fermi surface. The red and green lines in (b)(ii) indicate the position of the maximum intensity.

| 2nd Brillouin Zone | 3rd Brillouin Zone | 4th Brillouin Zone |
|-------------------|-------------------|-------------------|
| Peak position     | Peak amplitude    | Peak Gaussian linewidth |
| (a.i)             | (b.i)             | (c.i)             |
| (a.ii)            | (b.ii)            | (c.ii)            |
| (a.iii)           | (b.iii)           | (c.iii)           |

were then extracted from these spectral functions and are presented in figures 3 and 4. Spectral functions obtained using the semi-empirical model described in the methods section were also analyzed in a similar manner and are overlayed on the data in figures 3 and 4.

The experimental data obtained from the first Brillouin zone (position A–C from figure 2) is presented in figure 3. This data is compared to a semi-empirical model which involves 15 rotational domains equally spaced between $\pm 0.15^\circ$. The size (peak position) and intensity (peak amplitude) of the Fermi surface is well described by the model. The anisotropy in the width of the Fermi surface (variation in the peak Gaussian linewidth) is clearly evident by the ‘peanut’ shape in figures 3(a)(iii), (b)(iii) and (c)(iii) for both vacuum grown and argon grown samples. The ‘peanut’ shape is only produced by the semi-empirical model by considering rotational disorder. The size of the ‘peanut’ lobes is directly proportional to the rotational variation of the domains, with $\pm 0.15^\circ$ providing the best agreement. The number of domains included was also investigated, using more than five made no difference to the linewidth variation, while less than three and the Fermi surfaces from each domain where clearly
separated. A minimum of ten domains were required to adequately describe the lineshapes observed in figure 2(c), the value of 15 was therefore chosen to ensure a good agreement, however we cannot distinguish the exact size or number of domains imaged except when less than three are present.

Due to the six-fold symmetry the first Brillouin zone $K$ points are all equivalent with respect to the proposed rotational disorder. This is not the case for the higher order Brillouin zones (BZ2, BZ3 and BZ4 in figure 2) where the axis of rotation no longer lies in the $\Gamma K$ direction. Investigation of the higher Brillouin zone experimental spectral functions (presented in figure 4) then provides an important test of the rotational disorder model. The size (peak position) and intensity (peak amplitude) of the Fermi surfaces at each of the higher Brillouin zone locations are again well described by the rotational disorder model (15 domains, $\pm 0.15^\circ$ rotational spread). In particular figure 4(b)(ii) indicates that the experimental Fermi surface intensity has a maximum at $\sim 190^\circ$ (dash dot dot, light green, line) rather than the expected $180^\circ$, which is predicted by the rotational disorder model (dash dot, red, line).

The ‘peanut’ shape of the Fermi surface anisotropy (figure 4(a)(iii)) is observed in the second Brillouin zone, However this becomes more oval shaped in the third (b)(iii) and fourth (c)(iii) Brillouin zones as the axis of rotational disorder no longer aligns with the intensity anisotropy axis [5]. This variation is also well described by the rotational disorder model.

Further evidence for the rotational disorder is found in experimental Fermi surface intensity profiles (dashed lines) in the $KK$ and the $\Gamma K$ directions (figure 2(c)) taken from three distinct regions on an argon grown sample. The intensity profile from the semi-empirical model, with the $\pm 0.15^\circ$ rotational disorder, is overlayed in red (solid line). The spectra were obtained from the first Brillouin zone $K$ point and show a similar width and shape in the $\Gamma K$ direction (figures 2(c)(ii), (iv) and (vi)). In contrast three distinct line shapes are observed in the $KK$ direction (figures 2(c)(i), (iii) and (v)).

The most commonly observed lineshape across several samples is shown in figure 2(c)(i) and is well described by the rotational disorder model (15 domains within the $\pm 0.15^\circ$ rotational spread). The other two spectra are rare compared to the $\pm 15^\circ$ rotationally disordered spectra but provide a significant insight. In figure 2(c)(iii) an asymmetric line shape is observed. This asymmetry is described by a model including only two rotational domains ($\pm 0.15^\circ$ rotated) with an intensity ratio of 2:1 between them. The final region (figure 2(c)(v)) has a similar lineshape in the $KK$ and $\Gamma K$ direction, corresponding to a region containing only a single rotation.

Comparison of experimental angle resolved photoemission spectra from ‘vacuum grown’ and ‘argon grown’ epitaxial graphene on SiC(0001) to a semi-empirical model confirms the existence of a $\leq \pm 0.15^\circ$ rotational disorder of the Fermi surface. This disorder is attributed to a number of rotated graphene domains within the 50 $\mu$m photon beam size. Experimental data from regions of a vacuum grown sample which show only one and two rotational domains are also presented, however these are rare compared to the $\pm 0.15^\circ$ rotationally disordered spectra. Importantly the scale of the rotation ($\pm 0.15^\circ$) is very difficult to analyze by modern imaging techniques, such as low energy emission spectroscopy, photoelectron spectroscopy and scanning tunneling microscopy, and the common diffraction techniques, low energy electron diffraction and reflection high energy electron diffraction. It is therefore shown that detailed analysis of ARPES features can provide information on small scale structure variations not possible until now.
Acknowledgments

The Advanced Light Source is supported by the Director, Office of Science, Office of Basic Energy Sciences, of the US Department of Energy under contract no. DE-AC02-05CH11231. Work in Erlangen was supported by the ESF program EuroGRAPHENE and by the DFG priority program 1459 Graphene. AW acknowledges support from the Max Planck Society. KSK acknowledges support by NRF Grant funded by the Korean Government (NRF-2011-357-C00022). LM acknowledges support by a grant from the Swiss National Science Foundation (SNSF) (project no. PA00P2-136420).

References

[1] Geim A K and Novoselov K S 2007 Nature Mater. 6 183
[2] Berger C et al 2004 J. Phys. Chem. B 108 19912
[3] Emtsev K V et al 2009 Nature Mater. 8 203
[4] Emtsev K, Speck F, Seyller T, Ley I. and Riley J 2008 Phys. Rev. B 77 155303
[5] Mucha-Kruczyński M, Tsyplyatyev O, Grishin A, McCann E, Fal’ko V, Bostwick A and Rotenberg E 2008 Phys. Rev. B 77 195403
[6] McChesney J, Bostwick A, Ohta T and Emtsev K 2008 arXiv:0809.4046v1
[7] Polini M, Asgari R, Borghi G, Barlas Y and Perep-Barnea T 2008 Phys. Rev. B 77 081411
[8] Hwang E and das Sarma S 2008 Phys. Rev. B 77 081412
[9] Bostwick A, Speck F, Seyller T, Horn K, Polini M, Asgari R, MacDonald A H and Rotenberg E 2010 Science 328 999
[10] Qi Y, Rhim S, Sun G, Weinert M and Li L 2010 Phys. Rev. Lett. 105 085502
[11] Gierz I, Henk J, Höchst H, Ast C R and Kern K 2011 Phys. Rev. B 83 121408
[12] Siegel D A, Park C-H, Hwang C, Deslippe J, Fedorov A V, Louie S G and Lanzara A 2011 Proc. Natl Acad. Sci. USA doi:10.1073/pnas.1100242108
[13] Kim S, Ihm J, Choi H and Son Y-W 2008 Phys. Rev. Lett. 100 176802
[14] Zhou S Y, Gweon G, Fedorov A V, First P N, DeHeer W A, Lee D, Guinea F, Neto A and Lanzara A 2007 Nature Mater. 6 770
[15] Bostwick A, McChesney J, Emtsev K and Seyller T 2009 Phys. Rev. Lett. 103 056404
[16] de Gail R, Goerbig M, Guinea F, Montambaux G and Castro Neto A 2011 Phys. Rev. B 84 045436
[17] Bostwick A, Ohta T, McChesney J, Seyller T and Rotenberg E 2007 Solid State Commun. 143 63
[18] Ostler M, Speck F, Gick M and Seyller T 2010 Phys. Status Solidi b 247 2924
[19] Bostwick A, McChesney J, Ohta T and Rotenberg E 2009 Prog. Surf. Sci. 84 380–413
[20] Bostwick A, Ohta T, Seyller T, Horn K and Rotenberg E 2006 Nature Phys. 3 36
[21] Walter A L, Nie S, Bostwick A, Kim K S, Moreschini L, Chang Y J, Innocenti D, Horn K, McCarty K F and Rotenberg E 2011 Phys. Rev. B 84 195443
[22] Sutter P, Sadowski J T and Sutter E 2009 Phys. Rev. B 80 245411

New Journal of Physics 15 (2013) 023019 (http://www.njp.org/)