The last 6 Gyr of dark matter assembly in massive galaxies from the Kilo Degree Survey

C. Tortora1, N.R. Napolitano2, N. Roy2,3, M. Radovich4, F. Getman2, L.V.E. Koopmans1, G. A. Verdoes Kleijn1, K. H. Kuijken5

1 Kapteyn Astronomical Institute, University of Groningen, P.O. Box 800, 9700 AV Groningen, the Netherlands
2 INAF – Osservatorio Astronomico di Capodimonte, Salita Moiariello, 16, 80131 - Napoli, Italy
3 Dipartimento di Scienze Fisiche, Università di Napoli Federico II, Comp. Univ. Monte S. Angelo, 80126 - Napoli, Italy
4 INAF – Osservatorio Astronomico di Padova, Vicolo Osservatorio 5, 35122 - Padova, Italy
5 Leiden Observatory, Leiden University, P.O. Box 9513, 2300 RA Leiden, the Netherlands

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ABSTRACT
We study the dark matter (DM) assembly in the central regions of massive early-type galaxies up to \( z \sim 0.65 \). We use a sample of \( \sim 3800 \) massive \(( \log M/\odot > 11.2 )\) galaxies with photometry and structural parameters from 156 sq. deg. of the Kilo Degree Survey, and spectroscopic redshifts and velocity dispersions from SDSS. We obtain central total-to-stellar mass ratios, \( M_{\text{dyn}}/M_\star \), and DM fractions, by determining dynamical masses, \( M_{\text{dyn}} \), from Jeans modelling of SDSS aperture velocity dispersions and stellar masses, \( M_\star \), from KiDS galaxy colours. We first show how the central DM fraction correlates with structural parameters, mass and density proxies, and demonstrate that most of the local correlations are still observed up to \( z \sim 0.65 \); at fixed \( M_\star \), local galaxies have larger DM fraction, on average, than their counterparts at larger redshift. We also interpret these trends with a non universal Initial Mass Function (IMF), finding a strong evolution with redshift, which contrast independent observations and is at odds with the effect of galaxy mergers. For a fixed IMF, the galaxy assembly can be explained, realistically, by mass and size accretion, which can be physically achieved by a series of minor mergers. We reproduce both the \( R_e - M_\star \) and \( M_{\text{dyn}}/M_\star - M_\star \) evolution with stellar and dark mass changing at a different rate. This result suggests that the main progenitor galaxy is merging with less massive systems, characterized by a smaller \( M_{\text{dyn}}/M_\star \), consistently with results from halo abundance matching.

Key words: galaxies: evolution – galaxies: general – galaxies: elliptical and lenticular, cD – galaxies: structure.

1 INTRODUCTION
Dark matter (DM) dominates the mass density of galaxies and clusters of galaxies. Its budget amounts to \( \sim 85 \) per cent of the total mass density of the universe (e.g., Abazajian et al. 2003; Adelman-McCarthy et al. 2008; Abazajian et al. 2009) and its imprint is found at cosmological scales along all cosmic history (e.g., Komatsu et al. 2011). The strongest constraints on the shapes and properties of DM haloes come from numerical simulations of (DM only) structure formation within the consensus cosmology framework, i.e. the \( \Lambda \)CDM model (Navarro et al. 1996; Navarro et al. 1997; Bullock et al. 2001; Macciò et al. 2008). However, more realistic models, which try to account for the effect of baryons on the DM distribution (e.g., Blumenthal et al. 1984; Gnedin et al. 2004; Wu et al. 2014) seem more compatible with observations (e.g., Gnedin et al. 2007; Napolitano et al. 2010) and make more realistic predictions on the expected DM fractions in the central galaxy regions (Ruszkowski & Springel 2009; Hilz et al. 2013; Wu et al. 2014).

Early-type galaxies (ETGs, ellipticals and lenticulars) contain most of the cosmic stellar mass of the universe, and represent the final stage of galaxy evolution. They hold the fossil record of the stellar and DM assembly through time, and, being the most luminous and massive galaxies, can be

* E-mail: ctortora@astro.rug.nl
studied in details out to large redshifts. In particular, since ETGs are thought to be the product of the transformation of late-type galaxies’ (LTGs), e.g. through the effect of merging and other feedback mechanisms, they are crucial to understand the processes that shape galaxies across time.

In this context it is important to trace the assembly of both the luminous and the dark components of these systems. E.g., the total stellar-to-dark mass ratio of ETGs depends strongly on the galaxy mass, and seems to be connected to the overall star formation efficiency (Benson et al. 2000; Marini & Hudson 2002; Napolitano et al. 2005; Mandelbaum et al. 2006; van den Bosch et al. 2007; Conroy & Wechsler 2009; Moster et al. 2010; Alabi et al. 2016). But DM rules also the central galaxy regions (Gerhard et al. 2001; Padmanabhan et al. 2004; Cappellari et al. 2006; Thomas et al. 2007; Cardone et al. 2009; Tortora et al. 2009; van Dokkum & Conroy 2010). The first systematic studies of the evolution of the central DM fraction with mass (or velocity dispersion), from a bottom-lighter (i.e., ‘lower-mass’) IMF for low mass systems to a bottom-heavier (i.e., ‘higher-mass’) IMF in massive galaxies could dilute (and even cancel) the “apparent” DM fraction trend with mass (e.g., Thomas et al. [2011]; Tortora et al. [2013]). However, once again, the scenario is far to be fully constrained as for the most massive galaxies some contrasting results point to unexpected low stellar mass-to-light ratios (M/L) and bottom-light IMFs have been found (Smith et al. 2015).

One way to interpret all these evidences in the context of the galaxy evolution is to check the persistence of these correlations at higher-redshift and find the epochs where these effects start to emerge. This implies a test on the assembly of both the dark and the stellar matter in galaxies, at epochs where a) both are in an early stage of their evolution and b) the freedom on some parameters (e.g. age, metallicity of stars, concentration of the DM haloes, etc.) is minimal.

In order to cover the full parameter space, including the look-back time, we need large galaxy samples. So far, most of the DM studies were limited to low-redshift samples, and only recently systematic analysis of high redshift samples have been started. In some cases the datasets are restricted to small samples and small redshift windows to evaluate the dependence of the galaxy DM content on redshift, as in the case of gravitational lenses [Auger et al. 2009, 2010; Tortora et al. 2010b; Sonnenfeld et al. 2013]. The first studies have given contrasting results (Faure et al. 2011; Ruff et al. 2011). The reason of the tensions among these latter studies probably resides in the paucity of the galaxy samples and differences in the model choices.

The first systematic studies of the evolution of the central DM fraction with redshift has been recently performed by [Beifiori et al. 2014] and [Tortora et al. 2014b], which provided evidences that high-\(z\) ETGs are less DM dominated than their local counterparts.

However, this line of investigations has just started and further independent analyses are needed, not only to constrain the overall evolution of central DM, but also to assess the correlations with structural parameters, mass and stellar density, and evaluate how these change as a function of redshift, within or not the non-universal IMF scenario. To make even a step forward into the previous analysis, we have applied the Jeans method discussed in Tortora et al. (2014b) to a state-of-the-art sample of galaxies covering a broad redshift range for which high quality imaging and internal kinematics were available, both necessary to characterize the stellar and total mass for these systems. We have gathered a sample of massive galaxies with high-quality imaging, measured structural parameters and stellar masses from the Kilo Degree Survey (KiDS). KiDS is one of the public surveys carried out with the VST telescope, which is characterized by the excellent image quality, thanks to the very good seeing (0.65 arcsec, on average, in the \(g\)-band) and a high depth in the \(r\)-band (\(\sim 25\) mag limiting magnitude).

The KiDS fields in the Northern galaxy cap partially overlap with SDSS–DR7 data sample and with BOSS@SDSS, which both provided the spectroscopic redshifts and central velocity dispersions for our galaxy sample. Jeans modelling was used to determine dynamical masses and total-to-stellar mass ratios, to be correlated with galaxy parameters and redshift. Our results are also compared with those from a) low-redshift (0.05 < \(z\) < 0.095) ETGs from the SPIDER (Spheroid’s Panchromatic Investigation in Different Envi-
environmental Regimes) project (La Barbera et al. 2010; Tortora et al. 2012), b) a spectroscopically selected sample of ETGs covering the range of redshifts $z \sim 0.4 - 0.8$ from the ESO Distant Clusters Survey (EDisCS; Saglia et al. 2010; Tortora et al. 2014b), and c) other results from literature (Arnouts et al. 1999; Ilbert et al. 2006), which single burst synthesis (SPS) theoretical models and data. Single burst fitting method between the stellar population likelihoods (Arnouts et al., in preparation). Details about the catalog extraction and data analysis see Roy et al., in preparation. We limit to a mass-completed sample of galaxies with $\log M_*/M_\odot > 11.2$, consisting of a total of 3778 galaxies with redshift $0 < z < 0.7$.

In the following subsections we will provide more details about the products of the analysis of the KiDS dataset and the dynamical procedure. In particular, in Section 2.2 we will describe how the structural parameters are determined. In Section 2.3 we will provide details about the derivation of the stellar masses and the dynamical Jeans modelling is discussed in Section 2.4. In Section 2.5 we will define the total-to-stellar mass ratio and DM fraction. Finally, in Section 2.6 we discuss how progenitor bias is taken into account.

2 ANALYSIS

2.1 KiDS and SDSS datasamples

The galaxy sample presented in this work is selected from the data included in the first, second and third data releases of KiDS presented in de Jong et al. (2015) and de Jong et al. (2017). The total dataset includes 156 KiDS pointings with the measured structural parameters presented in Roy et al. (2017, in preparation). We have identified about 22 million sources, including $\sim 7$ million which have been classified as high quality extended sources. We select those systems with the highest $S/N$ in the $r$-band images, $S/N_r \equiv 1/MAGERR_{AUTO} > 50$, with reliable structural parameters measured. This dataset includes aperture and total photometry, photometric redshifts and structural parameters.

To record spectral information, such as spectroscopic redshifts and velocity dispersions, this data-sample is cross-matched with two different SDSS samples, collecting a sample of galaxies with redshifts in the range $0 < z < 0.7$:

- **MPA-JHU-DR7.** For the lowest redshifts ($z < 0.2$) we base our analysis on the spectroscopic data from the seventh Data Release of the SDSS (DR7; Abazajian et al. 2009). In particular, we select those systems, getting redshifts and velocity dispersions from the MPA-JHU-DR7 catalog which consists of $\sim 928000$ galaxies of any type with redshifts $z \lesssim 0.7$. The cut in mass which we will perform later will remove almost all the late-type contaminants. Spectra are measured within fibers of diameter 3 arcsec.

- **BOSS-DRI10.** Data at redshift $z \gtrsim 0.2$ are taken from the SDSS-III/BOSS Data Release Ten (DR10, Ahn et al. 2014). Selection criteria are designed to identify a sample of luminous and massive galaxies with an approximately uniform distribution of stellar masses following the Luminous Red Galaxy (LRG; Eisenstein et al. 2011) models of Maraston et al. (2009). The galaxy sample is composed of two populations: the higher-redshift Constant Mass Sample (CMASS; $0.4 < z < 0.7$) and the Low-Redshift Sample (LOWZ; $0.2 < z < 0.4$). The total sample, which consists of 934000 spectra and velocity dispersions across the full SDSS area, starts to be incomplete at redshift $z \gtrsim 0.6$ and masses $\log M_*/M_\odot \gtrsim 11.3$. The fiber diameter is of 2 arcsec. Velocity dispersions are determined in Thomas et al. (2013), using Penalized PiXel Fitting (pPXF, Cappellari & Emsellem 2004) and GANDALF (Sarzi et al. 2006) on the BOSS spectra. These values are quite robust being, on average, quite similar to the measurements from independent literature (see Thomas et al. 2013 for further details).

The final sample consists of 4118 MPA-JHU-DR7 galaxies and 5603 BOSS-DRI10 galaxies, for a total of 9721 systems with structural parameters, spectroscopic redshifts and velocity dispersions. We limit to a mass-completed sample of galaxies with $\log M_*/M_\odot > 11.2$, consisting of a total of 3778 galaxies with redshift $0 < z < 0.7$.

2.2 Structural parameters

Galaxy structural parameters have been derived via accurate 2D surface photometry of the highest $S/N$ sample (La Barbera et al. 2008; 2010; Roy et al. 2017, in preparation). Surface photometry is performed using the 2DPHOT environment, an automatic computer code designed to obtain both integrated and surface photometry of galaxies in wide-field images. The software first produces a local PSF model from a series of identified sure stars. For each galaxy, this is done by fitting the four closest stars to that galaxy with a sum of three two-dimensional Moffat functions. Then galaxy snapshots are fitted with PSF-convolved Sérsic models having elliptical isophotes plus a local background value (see La Barbera et al. 2008 for further details). The fit provides the following parameters for the four wavebands: surface brightness at $R_e$, $m_e$, circularized effective radius, $R_e$, Sérsic index, $n$, total magnitude, $m_B$, axis ratio, $q$, and position angle. As it is common use in the literature, in the paper we use the circularized effective radius, $R_e$, defined as $R_e = \sqrt{R_{e,\text{maj}} R_{e,\text{min}}}$, where $R_{e,\text{max}}$ is the major-axis effective radius. For further details about the catalog extraction and data analysis see Roy et al., in preparation.

2.3 Stellar mass determination

To determine stellar masses, $M_*$, we have used the software Le Phare (Arnouts et al. 1999; Ilbert et al. 2006), which performs a $\chi^2$ fitting method between the stellar population synthesis (SPS) theoretical models and data. Single burst models from Bruzual & Charlot (2003), with different metallicities ($0.2 \leq Z/Z_\odot \leq 2.5$) and ages ($3 \leq \text{age} \leq \text{age}_{\text{max}}$ Gyr), and a Chabrier (2001) IMF is used. The Salpeter (1955) gives masses larger of a factor $\sim 1.8$ (Tortora et al. 2009; Swindle et al. 2011). The maximum age, $\text{age}_{\text{max}}$, is set by the age of the Universe at the redshift of the galaxy,
with a maximum value at $z = 0$ of 13 Gyr. To minimize the probability of underestimating the stellar mass by obtaining too low an age, following [Maraston et al. (2013)] we have applied age cutoffs to the model templates, allowing for a minimum age of 3 Gyr. Models are redshifted using the SDSS spectroscopic redshifts. We adopted the observed KiDS $ugri$ photometry (and related 1σ uncertainties) within a 6″ aperture of diameter, corrected for Galactic extinction using the map of [Schlafly & Finkbeiner (2011)]. Total magnitudes derived from the Sérsic fitting, $m_\text{S}$, are used to correct the outcomes of LE PHARE for missing flux. The single burst assumption, as well as the older stellar populations and metal-richer models are suitable to describe the red and massive galaxies we are interested in (Gallazzi et al. 2005; Thomas et al. 2005; [Tortora et al. 2009]). Among LE PHARE outputs, we will adopt best-fitted masses in this paper.

2.4 Dynamical modelling

Following the analysis in [Tortora et al. 2009] and [Tortora et al. 2012] we model the SDSS aperture velocity dispersion of individual galaxies using the spherical isotropic Jeans equations to estimate the (total) dynamical mass $M_{\text{dyn}}$ (which, we will also refer to as $M_\text{dyn}$) within $r = 1 R_e$. In the Jeans equations, the stellar density and the total mass distribution need to be specified. Thus, the stellar density is provided by the 2D Sérsic fit of the KiDS $r$-band galaxy images, and the total (DM + stars) mass is assumed to have the form of a Singular Isothermal Sphere (SIS), from which $M(r) \propto \sigma_{\text{SIS}}^2 r$ (corresponding to a 3D mass density slope $\gamma = 2$), where $\sigma_{\text{SIS}}$ is the model (3D) velocity dispersion.

The total mass density profile in the centre of ETGs flattens with galaxy mass ([Remus et al. 2012], Dutton & Treu 2014; Tortora et al. 2014a; Poci et al. 2017]; low-mass ETGs have steep mass density distributions consistent with those of stars (i.e. consistently with a constant $M/L$ profile), while shallower isothermal profiles has been found to provide a robust description of the mass distribution in massive ETGs (e.g., [Kochanek 1991], Bolton et al. [2006], Koopmans et al. [2006], Gavazzi et al. [2007], Bolton et al. [2008], Auger et al. [2009], Auger et al. [2010], Chae et al. [2014]; Oguri et al. [2014]). This “conspiracy” ([Rusin et al. 2003], Treu & Koopmans [2004], Koopmans et al. [2006], Gavazzi et al. [2007], Tortora et al. [2009], Auger et al. [2010]; Tortora et al. [2014a]) seems to be motivated also by theoretical arguments: an overall isothermal profile can be explained by a smaller amount of dissipation during the formation of such high-mass galaxies, if compared to lower-mass systems, where higher level of dissipation leads to a more prominent contribution from newly formed stars to the total mass density in the center, steepening their total density slope. ([Koopmans et al. 2006], Remus et al. 2013, Tortora et al. 2014a, Remus et al. 2017]. For further details on the systematics introduced by the particular mass density profile choice, one can refer to [Tortora et al. 2009] and [Tortora et al. 2012] (see also Cardone et al. 2009, Cardone & Tortora 2010, Cardone et al. 2011].

We will discuss the impact of a non-isothermal mass density profile and orbital anisotropy on our inferences in Section 4.3.

2.5 Dark matter content and rest-frame quantities

We characterize the mass content of an ETG by computing the de-projected total-to-stellar mass ratio $\frac{M_{\text{dyn}}(r)}{M_\star(r)}$, i.e. the ratio between dynamical and stellar mass in a sphere of radius $r$ and refer to the value assumed by this quantity at the effective radius $R_e$, i.e. $\frac{M_{\text{dyn}}(R_e)}{M_\star(R_e)}$, as the “central” total-to-stellar mass ratio. As the total dynamical mass includes both stars and DM, we will also use a related quantity, which makes explicit the DM fraction within $R_e$, defined as $f_{\text{DM}}(R_e) = 1 - \frac{M_\star(R_e)}{M_{\text{dyn}}(R_e)}$. When not stated explicitly, $M_\star$ is referred to the SPS value assuming a Chabrier IMF, discussed in Section 2.3. Note that usually dynamical analysis formalisms include de-projected masses (e.g. see [Tortora et al. 2009]), while projected masses are typically present in strong lensing equations (e.g., [Auger et al. 2010]). The projected $M_{\text{dyn}}/M_\star$ or $f_{\text{DM}}$ are always larger than their de-projected versions within the same radius, because of the contribution of the outer parts of the halo along the line-of-sight. In the following, we will discuss the DM quantities described above as a function of structural parameters, masses, velocity dispersion, stellar density and, mainly, as a function of the redshift.

In the spherical Jeans equation, for the stellar density we have adopted the observed $r$-band structural parameters, while $\frac{M_{\text{dyn}}(R_e)}{M_\star(R_e)}$ are computed using rest-framed $n$ and $R_e$. Indeed, the effective radii should be referred to a fixed rest-frame wavelength to account for the effect of color gradients, which make ETG optical $R_e$ larger in bluer than in redder bands, on average. If this effect is not taken into account, then $R_e$ are systematically larger at higher redshift ([Sparks & Jorgensen 1993], [Hyde & Bernardi 2009a], [La Barbera & de Carvalho 2009], [Roche et al. 2010], [Beifiori et al. 2014], [Tortora et al. 2014b], [Vulcani et al. 2014]). Similar considerations hold for the Sérsic indices. In particular, using a sample of galaxies with $z < 0.3$, [Vulcani et al. 2014] estimate an increase from $g$ to $u$ and from $r$ to $g$-band of $\lesssim 15$ per cent, and similar results are found in [La Barbera & de Carvalho 2009] following the method in [Sparks & Jorgensen 1993]. We have determined the rest-frame structural parameters ($X = R_e$ and $n$) by interpolating the observed X parameters in the three KiDS wavebands $g, r$ and $i$. We have performed a linear fit

$$\log X = a + b \log \lambda,$$  \hspace{1cm} (1)



3 The projected stellar mass within $R_e$ is $0.5 \times M_\star$, while the de-projected stellar mass within the same radius is about $0.416 \times M_\star$ (calculated using a Sérsic profile with $n = 4$). Instead, for a SIS, the projected mass is $\pi/2$ times the spherical mass, and this value is constant with radius. Therefore, the projected total-to-stellar mass ratio is $\sim 1.3$ times (i.e. $\sim 0.12$ dex) larger than the equivalent de-projected quantity.
2.6 Progenitor bias

The results need to be corrected for progenitor bias, since low-z ETG samples contain galaxies that have stopped their star formation only recently and that would not be recognized as ETGs at higher redshifts. This is the case of systems with relatively young ages that cannot correspond to passive objects at higher-z (van Dokkum & Franx 2001; Saglia et al. 2010; [Beifiori et al. 2014]).

The impact of the progenitor bias can push galaxy parameters in different directions, as discussed in [Tortora et al. 2014b] E.g., the correlation of $R_e$ with galaxy age is still controversial. In fact, contrasting results are found by observational analysis, which show that, at fixed mass or velocity dispersion, younger systems are larger (Shankar et al. 2010) or also smaller (Shankar et al. 2010). There are results showing that younger galaxies are larger (Khocharf & Silk 2006) or also smaller (Shankar et al. 2010) than the oldest systems.

To correct for the progenitor bias we would need an accurate estimate of the galaxy ages. Unfortunately our galaxy age have been obtained from the fitting of spectral models to our KiDS optical multi-band photometry, hence they cannot be more than a qualitative guess. Thus, following (Beifiori et al. 2014), we remove those galaxies whose age and redshift $z = 0.65$ – the centre of our highest redshift bin – was less than 3 Gyr, which is the time needed for a typical galaxy to become passive. This cut leaves 2595 galaxies, i.e. about 69 per cent of the total sample. In the rest of the paper, because of the uncertainties in our photometric ages, we will discuss both the results without and with this progenitor bias correction.

3 CORRELATION WITH STRUCTURAL PARAMETERS AND MASS PROBES

3.1 Dark matter fraction

Fig. 1 shows central $M_{\text{dyn}}/M_*$ as a function of different galaxy parameters, i.e. effective radius, Sérsic index, velocity dispersion, stellar and dynamical mass, and central average de-projected stellar density, $\langle \rho_\star \rangle$, defined as $\langle \rho_\star \rangle = M_\star (R_e)/(4\pi R_e^3)$. Since here we have fixed the IMF to Chabrier, the $M_{\text{dyn}}/M_*$ trend implies a variation in the DM content. Red symbols are for the KiDS sample, where we have collected all the galaxies with redshift $z < 0.7$. Dashed blue lines with light blue shaded regions are for a sample of ETGs with redshifts 0.05 $< z < 0.059$ from the SPIDER survey, assuming $g$-band structural parameters. Error bars and the shaded regions are the 25–75 per cent quantiles. We will also fit the power-law relation $M_{\text{dyn}}/M_* \propto X^\alpha$, where $X$ is one of the galaxy parameters ($R_e$, $n$, $\sigma_\star$, $M_\star$, $\langle \rho_\star \rangle$, $M_{\text{dyn}}$) and $\alpha$ is the slope of the correlation. All the correlations are significant at more than 99 per cent.

We find a tight and positive correlation with a slope $\alpha = 0.72$ between $M_{\text{dyn}}/M_*$ and $R_e$, which is interpreted as a physical aperture effect, where a larger $R_e$ subtends a larger portion of a galaxy DM halo. A similar steep correlation also holds between $M_{\text{dyn}}/M_*$ and Sérsic index ($M_{\text{dy}}n/M_* \propto n^{0.92}$), which means that galaxies with steeper light profiles have higher central DM fractions. The galaxies with the smallest $R_e$ (10 $\sim 5$ kpc) and Sérsic indices (2) have the smallest DM fraction (15 per cent), while the largest galaxies ($R_e \sim 35$ kpc) with the steepest light profiles ($n \sim 10$) present the largest DM content (15 per cent).

We also find that $M_{\text{dyn}}/M_*$ correlates with $\sigma_\star$ ($M_{\text{dy}}n/M_* \propto \sigma_\star^{-0.89}$). Galaxies with larger $M_{\text{dyn}}$, i.e. with a larger content of bothstellar and dark matter, have a larger DM content ($M_{\text{dy}}n/M_* \propto 10$ i.e. 0.90 per cent of DM), the slope of the correlation is 0.7. The correlation with $M_\star$ is shallower, with an average $M_{\text{dy}}n/M_* \propto 3$ (i.e. 67 per cent of DM) and $\alpha = 0.11$.

Fig. 1 also shows a sharp anti-correlation between DM content and central average stellar density with $\alpha = -0.28$, which has been reported for the first time in Tortora et al. (2012), and now is confirmed using samples of intermediate-redshift galaxies. Galaxies with denser stellar cores have lower DM fractions (i.e. $M_{\text{dy}}n/M_* \propto 2$ or $\rho_\star \propto 0.5$ at $\rho_\star \sim 10^5 M_\odot$ kpc$^{-3}$), while $\rho_\star$ values as high as $\sim 0.95$ are found at the lowest densities ($\rho_\star \sim 10^5 M_\odot$ kpc$^{-3}$). This trend results from the fact that, on average, higher stellar densities correspond to smaller effective radii, implying a lower $M_{\text{dy}}n/M_*$. All these trends are qualitatively consistent with those found for a sample of massive $z \sim 0$ SPIDER galaxies (blue lines with shaded regions; see also Tortora et al. 2012). Our results confirm most of the previous literature at $z \sim 0$ (e.g. Padmanabhan et al. 2004; [Cappellari et al. 2006]; [Hyde & Bernardi 2009a]; [Tortora et al. 2009]; [Napolitano et al. 2010]; [Tortora et al. 2012]), or at intermediate redshift (Tortora et al. 2010b; [Auger et al. 2010]; [Tortora et al. 2014b]).

In Fig. 1 we also plot the results when progenitor bias is accounted for (dashed lines), showing that the trends are almost unaffected. We have finally plotted the results for two redshift bins: $0.1 < z \leq 0.3$ (purple solid line) and $0.3 < z \leq 0.7$ (darker red line). Excepted for the correlations with $R_e$ and $\langle \rho_\star \rangle$, we find an evolution in the $M_{\text{dyn}}/M_*$ with larger DM fraction in the lower redshift bin. Note that the median $M_{\text{dy}}n/M_*$ of the $z \sim 0$ SPIDER galaxies are smaller than those of KiDS galaxies in the lower redshift bin with $0.1 < z \leq 0.3$. This seems to contract the trend of higher $M_{\text{dy}}n/M_*$ at lower redshift just discussed and shown in Fig. 1. However, we caution the reader that this discrepancy can arise from differences in the sample selection and the analysis of the datasets, as such as the determination of stellar masses, which are determined using different apertures for magnitudes, sets of filters and spectral templates (see Section 4.3 for further details). We will come back to the dependence on the redshift in Section 4.

We have also compared our results with $M_{\text{dy}}n/M_*$ estimates from gravitational lensing and velocity dispersion of SLACS lenses ([Auger et al. 2009]; [2010]). We have taken lenses with log $M_\star/M_\odot > 11.2$ and an average redshift of $z \sim 0.2$. Lensing data needed to be homogenized in order to be compared with our $M_{\text{dy}}n/M_*$ values in Fig. 1.
SPIDER and KiDS datasamples. The origin of these discrepancies, where SLACS galaxies have sizes concentrated to within their rest-frame effective radius, must be linked to their fitted mass density, since their fitted mass-follows-light model and calculate the mass within their rest-frame effective radius, following a SIS model, which is on average a good approximation on sizes of galaxies of similar stellar mass can reside on the assumption of a de Vaucouleurs (1948) profile adopted by Auger et al. (2009) for their surface photometry fit. It is known that larger Sérsic values (typical of Massive ETGs) produce $R_e$s which are larger of the de Vaucouleurs values of $\sim 0.2$ dex or more (Tortora et al. 2012).

In panel (c) of Fig. 1 we also plot the results from Thomas et al. (2011), which make use of Schwarzschild’s orbit superposition technique in axisymmetric potentials to a sample of 16 COMA ETGs. We consider their results for a mass-follows-light model and calculate the mass within their rest-frame effective radius, following a SIS model, which is on average a good approximation on sizes of galaxies of similar stellar mass can reside on the assumption of a de Vaucouleurs (1948) profile adopted by Auger et al. (2009) for their surface photometry fit. It is known that larger Sérsic values (typical of Massive ETGs) produce $R_e$s which are larger of the de Vaucouleurs values of $\sim 0.2$ dex or more (Tortora et al. 2012).

In panel (c) of Fig. 1 we also plot the results from Thomas et al. (2011), which make use of Schwarzschild’s orbit superposition technique in axisymmetric potentials to a sample of 16 COMA ETGs. We consider their results for a mass-follows-light model and calculate the mass within their rest-frame effective radius, following a SIS model, which is on average a good approximation on sizes of galaxies of similar stellar mass can reside on the assumption of a de Vaucouleurs (1948) profile adopted by Auger et al. (2009) for their surface photometry fit. It is known that larger Sérsic values (typical of Massive ETGs) produce $R_e$s which are larger of the de Vaucouleurs values of $\sim 0.2$ dex or more (Tortora et al. 2012).
adopted by Thomas et al. (2011), have been obtained fitting a de Vaucouleurs profile (Jørgensen et al. 1995; Mehlert et al. 2000), which can be again the reason of the observed discrepancy as their underestimated $R_e$ might have produced smaller $M_{\text{dyn}}/M_\ast$.

Our derivation of $f_{\text{DM}}$ yields some cases where galaxies have unphysical $f_{\text{DM}} < 0$, since $M_{\text{dyn}}(R_e) < M_\ast(R_e)$. We find that only ~6 per cent of our galaxies have negative DM fractions. Using a Salpeter IMF we would have obtained smaller DM fraction, and for ~23 per cent even negative. We also find that these numbers are changing with redshift, with ~1, 3 and 12 per cent of negative $f_{\text{DM}}$ in the redshift bins $0.1 < z \leq 0.3$, $0.3 < z \leq 0.5$ and $0.5 < z \leq 0.7$. These fractions translate to ~5, 18 and 34 if a Salpeter IMF is adopted. This is a well known critical effect also discussed in previous works (see e.g. Tortora et al. 2009; Napolitano et al. 2010; Tortora et al. 2012). However, although a fraction or almost all of these negative $f_{\text{DM}}$ could be compatible with observational scatter in $M_\ast$ and $M_{\text{dyn}}$ (see Napolitano et al. 2010), it does not leave a complete freedom on the assumption of the IMF to adopt. In particular, higher stellar $M/L$ normalizations are unphysical for those systems which tend to have smaller $f_{\text{DM}}$ (e.g. the ones with smaller sizes and dynamical masses, larger stellar densities, higher redshift, etc.). In principle, one can ask whether by releasing the concept of the universal IMF it is possible to interpret all the trends of the mass excess in the central regions with a stellar mass excess (i.e. an IMF variation) rather than DM excess (i.e. $f_{\text{DM}}$ variation) with galaxy parameters as in Fig. 1 (e.g. Tortora et al. 2009; 2012; 2013; Spiniello’s thesis, Chapter 2).

### 3.2 Constraining the IMF

In this section we want to consider the case of a non-universal IMF and correlate the IMF variation with galaxy parameters. The IMF has been initially considered as universal across galaxy types and cosmic time, mostly because of a lack of evidence of variations among stellar clusters and OB associations in the Milky Way (see Bastian et al. 2010 for a review about IMF studies). This assumption has been recently questioned by different dynamical, lensing, and stellar population studies, finding evidence for systematic IMF variations in ETGs (Treu et al. 2010; Thomas et al. 2011; Conroy & van Dokkum 2012; Cappellari et al. 2012; 2013; Spiniello et al. 2012; Wegner et al. 2012; Dutton et al. 2013; Ferreras et al. 2013; Goudreau & Kruisjesen 2013; La Barbera et al. 2013; Tortora et al. 2013; Weidner et al. 2013; Goudreau & Kruisjesen 2014; Shi et al. 2015; Tortora et al. 2014a; 2014b; Martín-Navarro et al. 2015; Lyubenova et al. 2016; Tortora et al. 2016; Corsini et al. 2017; Li et al. 2017; Sonnenfeld et al. 2017). Following Tortora et al. 2012 and motivated by all the results pointing to a non-universal IMF (see in particular Tortora et al. 2014a), we can check how large the IMF has to be to cancel the presence of DM within 1 $R_e$. We estimate the expected variation of stellar mass normalization, defining the mismatch parameter $\delta_{\text{IMF}} \equiv M_\ast,\text{IMF}(R_e)/M_\ast(R_e)$, relative to a Chabrier IMF, where $M_\ast$ is the stellar mass estimated with a Chabrier IMF and $M_\ast,\text{IMF}$ is the stellar mass for any other IMF assumption. We can also define the related DM fraction as the one obtained for the particular IMF assumed, i.e. $f_{\text{DM}} = 1 - M_\ast,\text{IMF}(R_e)/M_{\text{dyn}}(R_e)$. The estimated $\delta_{\text{IMF}}$ with the assumption $f_{\text{DM}} = 0$ is substantially the $M_{\text{dyn}}/M_\ast$ plotted in Fig. 1 but with $M_{\text{dyn}} = M_\ast,\text{IMF}$. The IMF mismatch parameter corresponding to $f_{\text{DM}} = 0$ represents an extreme upper limit, since in the CDM a non-zero DM fraction is found also when accounting for a non-universal IMF (see e.g. Cappellari et al. 2013; Tortora et al. 2013). Hence, to explore more realistic dark matter fractions, we have also computed the IMF mismatch corresponding to $f_{\text{DM}} = 0.2$ or $f_{\text{DM}} = 0.4$, which bracket the typical values of the DM fraction found in SPIDER ETGs, when a free IMF normalization is adopted (Tortora et al. 2013). By construction, for the $f_{\text{DM}} = 0.2$ and 0.4 cases, our $M_{\text{dyn}}/M_\ast$ give a mass budget in stars, and thus $\delta_{\text{IMF}}$ values, which are systematically lower than the $f_{\text{DM}} = 0$ case.

To derive inferences about the IMF slope, we compare this dynamical $\delta_{\text{IMF}}$ with what is expected from stellar population models. Thus, we consider three power-law IMFs, with slopes 1.35 (i.e. Salpeter), 1.85, and 2.05 (i.e. a very bottom-heavy IMF). The $\delta_{\text{IMF}}$ is estimated as the ratio of the stellar $M/L$ between two SSPs having a power-law and a Chabrier IMFs, respectively. We compute the stellar K-band $M/L$, adopting the Bruzual & Charlot (2003) synthesis code, for old (10 Gyr) SSPs, with solar metallicity (see Tortora et al. 2012).

Fig. 2 plots the $\delta_{\text{IMF}}$ trends, for three different assumptions of the DM fraction, as a function of $R_e$, n, $\sigma_\text{c}$, $M_\ast$, and $M_{\text{dyn}}$ (red symbols). We compare the results against the $\sim 0$ estimate from SPIDER for $f_{\text{DM}} = 0$. Horizontal lines mark $\delta_{\text{IMF}}$ for the different IMFs obtained from stellar population synthesis. The intersections with the horizontal lines define the values of $R_e$, n, $\sigma_\text{c}$, $M_\ast$, and $M_{\text{dyn}}$, for which a given IMF slope would imply $f_{\text{DM}} = 0$, 0.2 and 0.4.

The figure shows that, in order to account for the apparent trend of $f_{\text{DM}}$ with $R_e$, n, $\langle \rho_\ast \rangle$ and $M_{\text{dyn}}$, galaxies with the largest radii, Sérsic indices and dynamical masses and the lowest $\langle \rho_\ast \rangle$ should have an IMF slope as steep as (or steeper than) 2.05 (e.g. Tortora et al. 2013; Tortora et al. 2014a; Spiniello et al. 2015). While at the lowest values of $R_e$, n and $M_{\text{dyn}}$, and highest $\langle \rho_\ast \rangle$, a Salpeter (Chabrier) IMF would be required if $f_{\text{DM}} = 0$ ($f_{\text{DM}} = 0.4$). Interestingly, in our mass range, $\delta_{\text{IMF}}$ is almost constant with stellar mass and is consistent with a slope $\sim 1.8$ when $f_{\text{DM}} = 0$, and with a Salpeter IMF if $f_{\text{DM}} = 0.4$. Despite the adopted constant $f_{\text{DM}}$, the trends with the parameters remain qualitatively the same and just shifted toward a lower normalization for higher $f_{\text{DM}}$ values.

However, IMFs with slopes $x \geq 2$ are disfavored in SLACS gravitational lenses, since they give stellar $M/L_s$ which violate the total mass inside the Einstein radius, i.e. within $R_e/2$ (Spiniello et al. 2012). Thus, the assumption of no DM within $R_e$ is not realistic and would be at odds with other results using gravitational lensing, too (see also later on in the paper).

Before starting to drive conclusions, we need to check how our assumptions might affect the main results of our analysis. All sources of systematics will be discussed in Section 4.3 however here we start showing the effect of unaccounted colour gradients and the galaxy model, using the SPIDER sample. For this sample we show the K-band results as dashed blue lines in Fig. 2 which provide smaller $\delta_{\text{IMF}}$ of about 0.2 dex, but with trends that are almost un-
In this section, we will first investigate the evolution of size and DM fraction as a function of redshift, at fixed stellar mass, comparing the results with some literature and predictions from different galaxy evolution scenarios. Then, to study in more detail the evolution of the mass and size in our galaxy sample, we compare some relevant correlations, as the ones between the galaxy size or DM fraction and $M_\star$, at different redshifts (Tortora et al. 2014b). In this latter case, we will create some toy-models to interpret this evolution in terms of physical processes.

4 EVOLUTION WITH REDSHIFT

A simple monolithic-like scenario, where the bulk of the stars is formed in a single dissipative event followed by a passive evolution, is no longer supported by the observations, while many observations suggest the occurrence of a strong mass and size evolution in ETGs (Daddi et al. 2005; Trujillo et al. 2006; Trujillo et al. 2007; Saglia et al. 2010; Trujillo et al. 2011; Tortora et al. 2014b). In this section, we will first investigate the evolution of size and DM fraction as a function of redshift, at fixed stellar mass, comparing the results with some literature and predictions from different galaxy evolution scenarios. Then, to study in more detail the evolution of the mass and size in our galaxy sample, we compare some relevant correlations, as the ones between the galaxy size or DM fraction and $M_\star$, at different redshifts (Tortora et al. 2014b). In this latter case, we will create some toy-models to interpret this evolution in terms of physical processes.
4.1 Evolution at fixed mass

Following some previous studies about size and velocity dispersion evolution we investigate how $R_e$, $σ_e$ and $M_{\text{dyn}}/M_\star$ change in terms of redshift, at fixed stellar mass. We concentrate our attention on two particular stellar mass bins ($11.2 < \log M_\star/M_\odot \leq 11.4$ and $11.4 < \log M_\star/M_\odot \leq 11.6$). Almost all the correlations discussed are significant at more than 99 per cent. In Fig. 3 we first plot the dependence of $R_e$ with the redshift (panels a and b), which show that sizes were smaller at earlier epochs of galaxy evolution (see Roy et al. in preparation, for further details about size evolution in KiDS galaxies). Following a standard approach in the literature, we fit the relation $R_e = R_{e,0}(1 + z)^α$ to the data. For the two mass bins, in the case of no progenitor bias correction (red filled squares with error bars), we find a slope, $α = −2.2$ and $−3.8$ respectively. These values translates into a weaker size evolution if we account for the progenitor bias (open squares with dashed red lines); in fact, the slopes become $α = −1.6$ and $−3.3$ in this case. These trends are steeper than the trends for spheroid- and disk-like systems with $M_\star > 10^{11} M_\odot$ taken from the literature (solid and dashed black lines in the top panels in Fig. 3) ([Trujillo et al. 2007; Buitrago et al. 2008; Conselice 2014]). At lower $z$ we find a good agreement with the $R_e$s from SPIDER dataset sample. However, we find some discrepancy in the size normalization with other analysis. For example, the 1-band measurements from EDisCS sample ([Saglia et al. 2000; Tortora et al. 2014b]), is lower of $0.3$ dex, while the 1-band $R_e$ in [Beifiori et al. 2014] re-calibrated using HST images, are smaller of a factor $0.2$ dex. The difference in the wavebands adopted (1-band $R_e$ in [Beifiori et al. 2014] vs our rest-frame $R_e$) cannot account for the observed large discrepancy. Overall, our results confirm the well known result that in massive galaxies the size of the galaxies is changing with redshift ([Daddi et al. 2005; Trujillo et al. 2006; Trujillo et al. 2007; Buitrago et al. 2008; van der Wel et al. 2008]).

In panels (c) and (d) of Fig. 3, we also plot the effective velocity dispersion, $σ_e$, as a function of the redshift. In this case the evolution with redshift is shallower, with higher-$z$ galaxies having slightly larger velocity dispersions ([Cenarro & Trujillo 2009; Posti et al. 2014]). In this case the evolution of $σ_e$ is quantified through the relation $σ_e = σ_{e,0}(1 + z)^α$ where the estimated slopes for the two mass bins above are $α = 0.21$ and $0.53$ (without progenitor bias) and $α = 0.46$ and $0.53$ (with progenitor bias) respectively. These results are in good agreement with local ([La Barbera et al. 2010; Tortora et al. 2012], intermediate-$z$ ([Beifiori et al. 2014] and higher-$z$ ([Saglia et al. 2010; Tortora et al. 2014b]) measures.

The total-to-stellar mass ratio (with a Chabrier IMF) is plotted in panels (e) and (f) of Fig. 3. The galaxies are DM dominated at lower redshift (i.e. 75–80 per cent of DM at $z \sim 0.2$), while $f_{\text{DM}}$ results to be smaller at higher-$z$ (40–50 per cent at $z \sim 0.6$). Fitting the $M_{\text{dyn}}/M_\star = (M_{\text{dyn}}/M_\star)_0(1 + z)^α$ relation to the data, for the two mass bins we find $α = −2.4$ and $−2.8$ (without progenitor bias) and $α = −1.3$ and $−2.2$ (with progenitor bias) respectively. We find a small discrepancy with SPIDER and EDisCS data sample, but these results agree within the data scatter. We also plot the $M_{\text{dyn}}/M_\star$ derived in [Beifiori et al. 2014], assuming a non-homologous constant-$M/L$ profile (with SDSS sizes recalibrated to HST values) as a solid cyan line. This latter model cannot be directly compared to our results because of its different assumption on the total mass distribution, hence we have re-scaled their $M_{\text{dyn}}/M_\star$ using the average ratio of the virial factors for SIS and constant-$M/L$ profile estimated in [Tortora et al. 2012]. After this re-normalization (solid cyan line in Fig. 3) the [Beifiori et al. 2014] estimates are on average consistent within 1 $σ$ scatter with the KiDS sample.

We want to interpret the trends of $σ_e$ and $M_{\text{dyn}}/M_\star$ in the context of galaxy evolution, by comparing the observed trends with the predictions from two different scenarios invoked to explain the galaxy size evolution. The merging scenario ([MS, hereafter]) predict that size is driven by the accretion of matter, with the result that the sizes of the merger remnants are larger than those of their remnants. The merging model of [Hopkins et al. 2009] predicts that the velocity dispersion varies in terms of the size as $σ_e(z) \propto (1 + γ)^{−1/2}$, while the $\gamma$ sets the DM contribution to the potential relative to that of the baryonic mass. This parameter varies between 1 and 2 (which are the best fitted values for $M_\star \sim 10^{11}$ and $10^{12} M_\odot$, respectively). Completely different is the "puffing-up" scenario ([PS, hereafter]) from [Fan et al. 2008], which predict that galaxies grow by the effect of quasar feedback, which removes huge amounts of cold gas from the central regions, quenching the star formation and increasing the size of the galaxy. This model predicts that velocity dispersion varies as $R_e^{−1/2}$.

To derive predictions in the above scenarios, we use as $R_e−z$ relation the interpolating line going through the KiDS median values in panels (a) and (b) of Fig. 3. This latter is inserted into the two equations discussed to derive the predicted velocity dispersions in the two schemes. Then we need to translate these predicted velocity dispersions into a $M_{\text{dyn}}/M_\star$. In order to do this we need first to derive the $M_{\text{dyn}}$ as a function of the redshift, solving the spherical Jeans equation, which contains 1) the density of the light distribution, 2) the total potential, 3) α as a function of redshift. For the light distribution we have taken the Sérsic profile with $n = 4$ for simplicity (i.e. a pure de Vaucouleurs) and with effective radius given by our interpolated $R_e(z)$ relation as defined above. For the total potential we have used the SIS profile. Then, we impose that the velocity dispersion derived from Jeans equation (averaged within $R_e$) equals the $σ(z)$ in the two scenarios, MS and PS. This procedure provides $M_{\text{dyn}}$ and $M_{\text{dyn}}/M_\star$ as a function of redshift. Note that what is relevant in this calculation is the trend with redshift and not the normalization, which is fixed by hand, since in the $σ_e(z)$ formulae the normalization factor is unspecified.

We plot the predicted trends for $σ_e$ and $M_{\text{dyn}}/M_\star$ in panels (c), (d), (e) and (f) of Fig. 3. The PS predicts a very strong evolution (with a change of $\sim 100$ km/s in the redshift window analyzed), which is discrepant with KiDS results for both the $σ_e$ and $M_{\text{dyn}}/M_\star$. On the contrary, the milder evolution from MS accommodates the observations. See a similar analysis for the $σ_e$ evolution in [Cenarro & Trujillo 2009], where similar conclusions are reached. However, while the agreement with the velocity dispersion seem very
Figure 3. Evolution with redshift of $R_e$ (panels a and b), $\sigma_e$ (panels c and d), $M_{\text{dyn}}/M_*$ (panels e and f) and $\delta_{\text{IMF}}$ (panels g and h) for two stellar mass bins: $11.2 < \log M_*/M_\odot \leq 11.4$ (left) and $11.4 < \log M_*/M_\odot \leq 11.6$ (right). Red symbols are as in previous figures. Open black square with error bar is median and 25–75th percentiles for SPIDER galaxies, while open black square is the median for the SPIDER sample when the progenitor bias is taken into account. Blue squares with bars are median and 25–75th percentiles for EDISCS sample. Cyan solid lines in panels (a), (c) and (e) are from Beifiori et al. (2014, B+14). In panel (e) the dashed line is calculated converting the results in Beifiori et al. (2014) assuming a constant-$M/L$ profile to a SIS profile, as explained in the text. The black solid and dotted lines in the top panels are taken from the average $R_e/R_{e,0}$-$z$ trends (with $R_{e,0} = R_e(z \sim 0)$) for spheroid-like galaxies in Trujillo et al. (2007, T+07) and disk-like systems in Buitrago et al. (2008, B+08), normalized to $R_{e,0} = 15$ and 11 kpc, respectively. Shaded gray region and green line are our predictions using the merging model of Hopkins et al. (2009, H+09) and the "puffing-up" scenario from Fan et al. (2008, F+08), respectively. See the text for further details. In the bottom panels (g and h), we show the $\delta_{\text{IMF}}$ when $f_{\text{DM}} = 0$ (filled squares), $f_{\text{DM}} = 0.2$ (filled circles) and $f_{\text{DM}} = 0.4$ (filled triangles), as in Fig. 2. Purple lines and shaded regions are the results obtained from the strong lensing and dynamical analysis of 80 ETGs in Sonnenfeld et al. (2015, S+15) and Sonnenfeld et al. (2017), the region sets the 68 per cent confidence level. The black star with error bars is for the average $\delta_{\text{IMF}}$ obtained by analyzing the kinematical data of a sample of 68 galaxies at $z \sim 0.75$ in Shetty & Cappellari (2014, S&C14). Horizontal lines correspond to the relative variation of stellar mass, $M_{*,\text{IMF}}/M_*$ with respect to a Chabrier IMF – as in Fig. 2. See legend at right, explanation in the main text, and the text in this caption for abbreviations.
good, the model predict a shallower $M_{\text{dyn}}/M_\star - z$ trend than the observed one, in both the mass bins.

Following the analysis made in Section 3, in panels (g) and (h) we also interpret the evolution of the $M_{\text{dyn}}/M_\star$ with redshift in terms of a change in the IMF and of DM content. We show how the mismatch parameter $\delta_{\text{IMF}}$ is changing in terms of redshift, for 3 different $f_{\text{DM}}$ values ($f_{\text{DM}} = 0$, 0.2 and 0.4). If we assume that $f_{\text{DM}}(R_e)$ is not changing with redshift, then the observed $M_{\text{dyn}}/M_\star$ evolution can be explained by a change of the IMF “normalization”. The $\delta_{\text{IMF}}$ values found for $f_{\text{DM}} = 0$ need to be considered as upper limits, and point to a Salpeter IMF at low redshift (with $z \approx 2.05$), if $f_{\text{DM}} = 0$. 

For the maximal DM fraction adopted here, i.e. $f_{\text{DM}} = 0.4$, KiDS results suggest a standard Chabrier IMF at $z \approx 0.65$ and slightly super-Salpeter at $z \approx 0$. If we consider that a more realistic situation would allow for a variation of $f_{\text{DM}}$ with redshift (e.g., from $f_{\text{DM}} = 0$ at $z \approx 0.65$ to $f_{\text{DM}} = 0.4$ at $z \approx 0$), then the $\delta_{\text{IMF}}$ evolution would result weaker or totally absent.

We finally compare our findings for $\delta_{\text{IMF}}$ with some results from the literature. Sonnenfeld et al. (2015) and Sonnenfeld et al. (2017) measure $\delta_{\text{IMF}}$ for a sample of 80 massive ETGs, using strong lensing and velocity dispersion data. We plot their 68 per cent confidence region with purple symbols in Fig. 3. Their trend is shallower than our results found assuming a constant $f_{\text{DM}}$ value. An agreement with these results can be found if we allow in our data for the more realistic $f_{\text{DM}}$ evolution discussed above, i.e. if we assume that $f_{\text{DM}}$ is null at $z \approx 0.65$ and $\geq 0.4$ at $z \approx 0$. The black star with error bars is the average $\delta_{\text{IMF}}$ from Shetty & Cappellari (2014), obtained through the dynamical modelling of kinematical data of a sample of 68 massive ($M_\star \geq 10^{11} M_\odot$) galaxies at $z \approx 0.75$, extracted from the DEEP2 spectrographic survey. As in our $f_{\text{DM}} = 0$ case, their results have to be considered as upper limits, since they assume that mass follows light and no DM at all is considered. Their estimate would be normalized to our mass model assumption. This would be done by adding a factor $\sim 0.14$ dex to covert a constant $M/L$ profile to a SIS (Tortora et al. 2012), but their value would be larger of $\sim 0.16$ dex if compared with the virial estimator, which they suggest to be related to underestimated $R_e$ in the virial estimator formula (see Cappellari et al. 2013; Shetty & Cappellari 2014). Thus, since these two factors would almost elide, we have decided to not add any corrective factor to their $\delta_{\text{IMF}}$ estimate shown in Fig. 3.

These results are about 0.1 dex larger than our $f_{\text{DM}} = 0$ findings at the same redshifts (see KiDS and EDisCS data points in Fig. 3).

As it has been done for the central DM evolution presented in panels (e) and (f) in Fig. 3, it would be interesting to interpret if this change of IMF with time is realistic and if is consistent with specific processes. In Tortora et al. (2014b) we proposed some speculative considerations, suggesting that a change of IMF with redshift could be produced by two different processes: (a) new stars formed in the galaxy center during a wet merging process, which also produce ‘higher mass’ IMF (Napolitano et al. 2010) and positive age gradients (Tortora et al. 2010a) in young and massive local ETGs, or (b) stars from both merging galaxies, which are characterized by two different IMFs, which can combine to modify the cumulative IMF of the merger remnant. Unfortunately, the net effect of these processes on the final IMF normalization is not yet clear, and in most cases the combination of a ‘higher’ and a ‘lower mass’ IMF would produce a diluted IMF. Thus, galaxy mergers would produce smaller $\delta_{\text{IMF}}$ values, or leave $\delta_{\text{IMF}}$ almost constant with redshift, as predicted by the galaxy merging toy-models in Sonnenfeld et al. (2017). These results contrast the strong evolution observed in panels (g) and (h) of Fig. 3.

All these results seem to suggest that most of the $M_{\text{dyn}}/M_\star$ evolution would be driven by a change of the DM fraction. A deeper analysis will be needed to constrain the IMF and DM fraction in term of redshift. In a future paper we will discuss this problem with more details.

4.2 Size, mass and DM evolution

The analysis performed in the previous section cannot be conclusive, since it does not take into account that in merging processes a single galaxy also changes in mass. For this reason, in Fig. 4 we compare the $R_e - M_\star$ and $M_{\text{dyn}}/M_\star - M_\star$ relations (assuming a fixed Chabrier IMF) for KiDS galaxies at different redshift and study the joint evolution of size and mass. We start seeing how lower redshift galaxies are larger and contain more DM in their cores at all values of $M_\star$, confirming the trends in Figs. 1 and 3. The trend is weaker if we consider the progenitors bias, which affects mostly the lowest redshift bin (dashed lines in Figs. 1 and 3). In the following we will try to reproduce these trends within the hierarchical framework. Galaxy mergers are the most accredited mechanisms that can account for both size and mass accretion, as we have also seen from the analysis of Section 4.1. Dissipationless major mergers from simulations in elliptical galaxies have predicted that the DM fraction within a certain physical radius decreases mildly after the merger (Boylan-Kolchin et al. 2005). But they have also shown that the DM fraction within the final $R_e$ is greater than the DM fraction within the initial $R_e$, because the total mass within $R_e$, $M_v(R_e)$, changes after the merger more than $M_v(R_e)$. We have found the same result with real data (Fig. 3; Tortora et al. 2014b) and we have also found in Fig. 4 that this is also the case for a toy-model which assumes the merging model from Hopkins et al. (2009) and the observed $R_e - z$ relation.

At different final stellar masses, they find that the equal-mass mergers produce a smaller size increase of multiple minor mergers. In particular, the variation of $R_e$ with respect to the initial radius, $R_e/R_0$, in terms of the variation of $M_\star$, with respect to the initial stellar mass, $M_\star/M_0$, is found to be $R_e/R_0 \propto (M_\star/M_0)^{0.91}$ for the equal-mass merger and $\propto (M_\star/M_0)^{2.4}$ for the minor mergers (consistently with what was observed by van Dokkum et al. 2010).

Taking these results into account, we have constructed some toy-models assuming $\eta_{\text{DM}} \propto M_v/R_e^{2+}$ around $R_e$, with $\eta \sim 2$ for a standard NFW and $\eta \sim 1.2$ for a contracted NFW, hereafter AC$+\text{NFW}$ (according with Boylan-Kolchin et al. 2005). Following Hilz et al. (2013), we have also taken the average evolution of $R_e$ in terms of $M_\star$ evolution for the equal-mass merging (i.e. $R_e/R_0 \propto (M_\star/M_0)^{0.91}$) and minor merging (i.e. $R_e/R_0 \propto (M_\star/M_0)^{2.4}$). Following Tortora et al. 2014b, we start assuming that the variation of the virial mass follows the one of the stellar mass, i.e.
$\delta M_{\text{vir}} \approx \delta M_\star$. This intrinsically reflects the hypothesis that the systems participating to merging (i.e. the progenitors) all have the same $M_{\text{vir}}/M_\star$, which is reasonable for most of the stellar mass range covered by our sample. However, it is possible - mainly for the minor merging case - that the virial mass change at a different rate of the stellar mass, since the main galaxy is merging with another galaxy with a different $M_{\text{vir}}/M_\star$ (see, e.g., Table 2 in Boylan-Kolchin et al. 2005 where the final virial mass after the mergers is changed less than total stellar mass). These simplified models provide a quantitative assessment of the impact of the merging scenario on the observed DM fraction.

We have considered the evolution tracks related to the two different merging types (major and minor) for a galaxy with $\log M_\star/M_\odot = 11.4$. Dots and squares are for NFW and AC+NFW profiles, respectively. In the left panels (a and b), the major merging tracks are shown as black lines with dots/squares indicating the events corresponding to masses $\delta M_\star \times M_{\text{star},0}$, with the mass increments $\delta M_\star = 1, 2, 4, ..., 0.5 \leq z \leq 0.7$. The first dot/square at $log M_\star/M_\odot = 11.4$ corresponds to the initial progenitor galaxy. The second dot/square is the result of one major merger, which doubles the initial mass of the progenitor, while the third dot/square corresponds to a second major merger with mass 4 times the mass of the initial progenitor and 2 times the mass of the remnant of the first merging event. The minor merging tracks are shown in the right panels (c and d) by black lines. Dots/squares indicate remnant with masses $M_{\text{star},0} + \delta M_\star \times M_{\text{star},0}$ where $\delta M_\star = 0, 0.2, 0.4, 0.6, ..., 0.5 \leq z \leq 0.7$. The solid lines are medians for the full sample, while dashed lines are for results corrected for progenitor bias. We take, as example, the average galaxy at $log M_\star/M_\odot = 11.4$ and evolve it accordingly to the toy-models discussed in the text. In the left (right) panels major (minor) merging predictions are shown. In the bottom panels (b and d), dots and filled squares are for NFW and AC+NFW profiles when $\delta M_\star = \delta M_{\text{vir}}$, and set the $R_{\text{vir}}, M_\star$ and $M_{\text{dyn}}/M_\star$ after each single merging event. In panel d, open circle and squares are for NFW and AC+NFW profiles when $\delta M_\star \neq \delta M_{\text{vir}}$.

Figure 4. Evolution of $R_{\text{vir}}-M_\star$ (panel a and c) and $M_{\text{dyn}}/M_\star-M_\star$ (panels b and d). Blue, green and red lines are for galaxies in three redshift bins $0.1 < z \leq 0.3, 0.3 < z \leq 0.5$ and $0.5 < z \leq 0.7$. Solid lines are medians for the full sample, while dashed lines are for results corrected for progenitor bias. We take, as example, the average galaxy at $log M_\star/M_\odot = 11.4$ and evolve it accordingly to the toy-models discussed in the text. In the left (right) panels major (minor) merging predictions are shown. In the bottom panels (b and d), dots and filled squares are for NFW and AC+NFW profiles when $\delta M_\star = \delta M_{\text{vir}}$, and set the $R_{\text{vir}}, M_\star$ and $M_{\text{dyn}}/M_\star$ after each single merging event. In panel d, open circle and squares are for NFW and AC+NFW profiles when $\delta M_\star \neq \delta M_{\text{vir}}$.
$M_{\text{dyn}}/M_\star$ evolution is too steep, thus after $\sim 2$ minor mergers the example galaxy would end up on the $z \sim 0.2$ observed $M_{\text{dyn}}/M_\star$, this number is not consistent with what found analyzing the $R_{\text{e}}/M_\star$ evolution, which would require $4-6$ mergers to transform the $z \sim 0.6$ galaxy in a typical galaxy observed at $z \sim 0.2$. The number of minor mergers needed to transform the $z \sim 0.6$ galaxy in a bigger and more DM-dominated galaxy is found if the DM mass is accreting with a lower rate and only for the AC+NFW mass profile. This is possible if the main progenitor is merging with lower mass galaxies with smaller $M_{\text{dyn}}/M_\star$. This result suggest that our massive galaxy at $z \sim 0.6$ has to merge with a population of less massive galaxies with lower total-to-stellar mass ratios. Abundance matching studies predict the existence of these systems, since at stellar masses smaller than $10^{11.4}$ $M_\odot$ galaxies are found to have, on average, smaller $M_{\text{dyn}}/M_\star$ (see e.g. Moster et al. [2010]).

4.3 Systematics

There are different sources of systematics that may impact our results. We will list some of these systematics in the following

(i) **KiDS vs. SPIDER.** We have cross-matched the full matched DR7 sample (5223 galaxies) with the SDSS-based SPIDER datasample (39993 galaxies), finding 248 galaxies with reliable structural parameters and masses in common. This sample spans the range of masses $\log M_\star/M_\odot \sim (10.2 - 11.4)$, which is different from the range used in this paper (i.e., $\log M_\star/M_\odot > 11.2$). We compare both structural parameters, stellar masses and velocity dispersions. Some differences are expected since the two samples rely on different image quality. Thus, while the median axis ratio is identical, and equal to $q_i = 0.7$, some small differences, are found between KiDS and SPIDER in the effective radius (3.2” vs. 2.9”) and S\ërsic index (5.6 vs. 5.3). The reason of this difference can probably be examined in the deepest KiDS images, which, including more light from the external regions, tend to produce larger sizes. However, these differences are within the typical measured uncertainties (see Roy et al. [2017], in preparation, for further details). Moreover, also stellar masses are consistent, with a median value of $\log M_\star M_\odot \sim 10.7$ dex. But, we caution the reader that KiDS and SDSS stellar masses are calculated using different photometric apertures (3 arcsec vs 3 times the $i$-band Kron radius), different wavelength coverage (optical vs. optical+IR) different stellar population prescription (single-bursts vs. exponential star formation). The aperture velocity dispersion is also consistent.

(ii) **Stellar mass modelling.** There are many systematics related to the stellar mass modelling. First of all, the $M_\star$ ($M_{\text{dyn}}/M_\star$) can become lower (higher) if we relax the constraints on age (e.g. by allowing ages lower than 3 Gyr) and metallicity (hence resuming the full BC03 synthetic library). The trends in terms of redshift are shallower, since the masses at larger redshifts are underestimated, as discussed in [Maraston et al. [2013]]. Then, we have seen that median masses from LE PHARE are smaller or $\sim 0.05$ dex if compared with the best-fitted values adopted in our analysis; however, the trends with redshift for $M_{\text{dyn}}/M_\star$ are quite similar. Then, stellar masses are negligibly affected if MAG_AUTO are adopted, instead of aperture magnitudes. The impact of stellar population templates is finally investigated for the BOSS datasample, comparing our inferences with BOSS values from [Maraston et al. [2013]]. These BOSS masses are obtained fitting [Maraston & Strömbäck [2011]] passive templates (with ages older than 3 Gyr) to the u, g, r, i, z BOSS magnitudes. We have re-normalized [Maraston et al. [2013]] stellar masses to a Chabrier IMF, by subtracting 0.05 dex, and converted to our cosmology by subtracting 0.035 dex, too. On average, our stellar masses are $\sim 0.08$ dex larger, this discrepancy is related to differences in datasample and template prescription adopted. However, the difference is also stronger at $z \lesssim 0.5$, i.e. $\sim 0.12$ dex, and is inverted at $0.6 \lesssim z \lesssim 0.7$, where our masses get smaller than BOSS estimates of $\sim 0.06$ dex. The trends of $M_{\text{dyn}}/M_\star$ stay qualitatively the same. Thus, the results of this paper do not change if different stellar mass estimates are adopted, and conclusions are unaffected.

(iii) **Stellar mass uncertainties.** The median uncertainty of the Chabrier-IMF stellar masses determined in Section 2.3 in our massive galaxy sample is $\sim 0.13$ dex. We studied the impact of these uncertainties on our mass selection and all the trends discussed in the paper. We have randomly perturbed each mass, assuming a Gaussian with as median the best-fitted mass and standard deviation the error of the best-fitted mass. Thus, we have selected the most massive galaxies with log $M_\star/M_\odot > 11.2$, using the new perturbed masses. The impact on the $M_{\text{dyn}}/M_\star - z$ trend is negligible.

(iv) **Stellar $M/L$ gradients.** We already shown how the gradients impact the results by comparing the g- and K-band results for the SPIDER sample in Section 3. However, in general, at masses log $M_\star/M_\odot > 11.2$ the colour and stellar $M/L$ gradients are weak, thus the correction would be small (Tortora et al. [2011]). Later analysis would also take into account possible gradients in the IMF (Martin-Navarro et al. [2015]).

(v) **Mass profile slope.** In addition to uncertainties in stellar mass estimates, the choice of the mass profile can be inappropriate for lower-$\sigma_\star$ (or $M_\star$) galaxies and cause an excess of negative $M_{\text{dyn}}/M_\star$ values, mainly at high-$z$ (e.g. Sonnenfeld et al. [2013]). In particular, $M_{\text{dyn}}/M_\star$ and the slope of total mass density are tightly correlated, with shallower density profiles corresponding to larger $M_{\text{dyn}}/M_\star$ (Humphrey & Buote [2010] Remus et al. [2013] Dutton & Tremonti [2014] Tortora et al. [2014a]). To quantify the impact of a free-varying total mass density slope, $\alpha$, we have adopted a power-law mass density $\rho \propto r^\alpha$, with slope steeper and shallower than isothermal. In Tortora et al. [2014b] we have shown that using two extreme values for the density slope, i.e. $\alpha = -2.5$ and $-1.5$, which bracket most of the results in the literature, then we find that the average $M_{\text{dyn}}/M_\star$ get smaller (larger) of $\sim 0.1$ ($\sim 0.05$) dex for $\alpha = -2.5$ ($-1.5$). However, in the realistic case with a varying slope with mass, smaller changes would be expected (Dutton & Tremonti [2014] Tortora et al. [2014a]). If $\alpha$ is constant with time, then, at fixed mass, these corrections would shift all the results of the same factor, leaving naturally unaffected the observed trend with redshift. On the other hand, if we assume that the slope is varying with redshift, then the only way to totally remove any $M_{\text{dyn}}/M_\star$ evolution is that low- and high-redshift galaxies have systematically steeper (i.e. $\alpha < -2.5$) and shallower (i.e. $\alpha > -1.5$) mass density profiles than isothermal, and
consequently smaller and larger $M_{\text{dyn}}/M_\ast$. However, this is not expected since the most massive galaxies are found to have only more shallow profiles than isothermal at lower redshifts (e.g. Tortora et al. 2014a, Poci et al. 2017) and at high redshifts, where gas and in situ star formation dominate the galaxy evolution, the ETGs from cosmological simulations have a total density slope very steep ($\alpha \sim -3$), with merging events driving the galaxy to a nearly isothermal profile (Remus et al. 2013, 2017; Xu et al. 2017) from the Illustris simulation find that a $\alpha$ is constant with redshift, which would leave the trend unaffected. While, using strong lenses, Bolton et al. (2012) and Sonnenfeld et al. (2013) have shown that the total mass density slope is steeper at lower redshift.

In particular, Sonnenfeld et al. (2013) find an average mass that the total mass density slope is steeper at lower redshift. Bolton et al. (2012) and Sonnenfeld et al. (2013) have shown would leave the trend unaffected. While, using strong lenses, we have a total density slope very steep ($\alpha \sim -3$), with merging events driving the galaxy to a nearly isothermal profile (Remus et al. 2013, 2017; Xu et al. 2017) from the Illustris simulation find that a $\alpha$ is constant with redshift, which would leave the trend unaffected. While, using strong lenses, Bolton et al. (2012) and Sonnenfeld et al. (2013) have shown that the total mass density slope is steeper at lower redshift.

(vi) Rotation velocity. We have also neglected rotation correction, not accounted by the aperture velocity dispersion. If rotation velocities would be included in the analysis $M_{\text{dyn}}$ would get higher. But the impact would be negligible if compared with typical uncertainties. In the massive and high velocity dispersion galaxies analyzed in this paper, this change would amount to $\sim 1$ per cent (see Tortora et al. 2009).

(vii) Orbital anisotropy. The DM content of ETGs is estimated under the assumption that their stellar orbits are isotropic, which is incorrect at some level. Detailed dynamical modeling analysis have focused on the ETG central regions, finding anisotropies to be fairly mild in general, typically in the range $-0.2 \leq \beta \leq +0.3$ (Gerhard et al. 2001, Cappellari et al. 2007), where $\beta \equiv 1 - \sigma_\parallel^2/\sigma_\perp^2$ quantifies the relative internal dispersions in the tangential and radial directions. Mild central anisotropy is also predicted from simulations of merger remnants (Dekel et al. 2005). The typical radial anisotropies found in local galaxies ($\beta \sim 0.2$), would decrease inferred dynamical masses by $\lesssim 5$ per cent (i.e. $\lesssim 0.02$ dex), lowering the $M_{\text{dyn}}/M_\ast$. Recently, using a sample of massive ($M_\ast > 10^{11} M_\odot$) galaxies in the Illustris simulation, [Xu et al. 2017] have predicted a gentle evolution in the average central anisotropy of their sample, from $\beta \sim -0.1$ at $z \sim 0.65$ to $\beta \sim 0.1$ at $z \sim 0.1$. This means that at $z \sim 0.1$ ($z \sim 0.65$) $M_{\text{dyn}}/M_\ast$ would be smaller (larger) of $\lesssim 3$ per cent ($\lesssim 3$ per cent), flattening our $M_{\text{dyn}}/M_\ast$-$z$ trend. However, the impact on our results is negligible.

(viii) Ellipticity. We have checked the effect of the ellipticity in the mass inferences and restricted the analysis to KiDS objects with axis-ratio $q > 0.6$ (86 per cent of the sample), in order to limit to the roundest galaxies. The overall results are practically unchanged.

(ix) Sérsic index selection. We have also checked if the results are affected if we select those objects with large Sérsic indices (i.e., r-band $n > 2.5$), typical of most of the ETGs (Tortora et al. 2010a). This high-$n$ sample consists of $\sim 94$ per cent of the original sample of massive galaxies. The impact on the results is negligible, too.

(x) Rest-frame structural parameters. We have derived rest-frame structural parameters by fitting a straight line $\log X = a + b \log \lambda$ to the datapoints ($\lambda_i, X_i$) at the three KiDS wavebands $g, r$ and $i$. To study the impact of this choice, we have also replaced the straight line with the polynomial function $\log X = a + b \log \lambda + c (\log \lambda)^2$. The impact on our results is negligible, since the difference between the derived Sérsic index, effective radius and $M_{\text{dyn}}/M_\ast$ using the two fitting functions are smaller than 3 per cent.

(xi) We do not include in the mass model the black hole, but we have calculated that its effect is, on average, negligible, with an impact on $M_{\text{dyn}}$ of $\sim 2$ per cent (Tortora et al. 2009).

5 CONCLUSIONS

We have analyzed the central DM content in a sample of massive ($\log M_\ast/M_\odot > 11.2$) ETGs at redshift $\leq 0.7$ from the Kilo Degree Survey, a VST public survey (de Jong et al. 2015, 2017). Thanks to the excellent seeing condition at Paranal, the small pixel scale (0.2′′ per pixel) and the depth of the survey, KiDS provides us with high quality images. We extract a sample of galaxies with $S/N > 50$, with masses and structural parameters from 156 sq. deg. of the KiDS survey, and spectroscopic coverage from SDSS-DR7 and BOSS@SDSS datasets. With spectroscopic redshifts, structural parameters, stellar masses, and velocity dispersion for a sample of 3778 massive ($\log M_\ast/M_\odot > 11.2$) galaxies, we can rely on the ideal dataset to perform the isotropic Jeans dynamical analysis and study the central DM content, parameterized through the total-to-stellar mass ratio, $M_{\text{dyn}}/M_\ast$, (calculated at $r = 1 R_e$; Tortora et al. 2009, 2012, 2014b).

We have shown that the local relationships between $M_{\text{dyn}}/M_\ast$ and effective radius $R_e$, Sérsic index n, velocity dispersion within effective radius $\sigma_e$, stellar mass $M_\ast$, central average stellar density ($\rho_c$) and dynamical mass $M_{\text{dyn}}$ conserve their trends at larger redshifts. These correlations are shown in Fig. 1. We find that larger galaxies with steeper light profiles (large n’s) are more DM dominated. The effective radius is the main driver of all the correlations. A similar steep trend is found in terms of $M_{\text{dyn}}$ and $\sigma_e$. On the contrary, $M_{\text{dyn}}/M_\ast$ vary weakly in terms of $M_\ast$, while we find a steep anti-correlation with central average stellar density. These results confirm most of the previous literature at $z \sim 0$ (Padmanabhan et al. 2004, Cappellari et al. 2006, Hyde & Bernardi 2009a, Tortora et al. 2009, Napolitano et al. 2010, Tortora et al. 2012), or at intermediate redshift (Tortora et al. 2010b, Anger et al. 2010, Barnabe et al. 2011, Tortora et al. 2014b).

However, one of the most important result of this paper is that the central DM is evolving from high $−$ low $z$, with less DM at higher redshift. At fixed mass, we find that the galaxies in the highest redshift bin have $M_{\text{dyn}}/M_\ast \sim 0.2$–0.4 dex smaller than local galaxies. Our findings are qualitatively consistent with results in Beifiori et al. 2014 and Tortora et al. 2014b. We have also investigated the evolution of $R_e, \sigma_e$ and $M_{\text{dyn}}/M_\ast$ within various galaxy formation scenarios. We exclude the "puffing-up" scenario from AGN feedback in Fan et al. 2008, since this kind of process produces very high $\sigma_e$ and $M_{\text{dyn}}/M_\ast$ at higher $− z$, not observed. The predictions from galaxy merging scenario from Hopkins et al. 2009 is consistent with the observed size and mass growth with $z$ (Fig. 3).

We find that the fraction of galaxies with negative DM is increasing with redshift, but for the massive galaxies under analysis a Chabrier or Salpeter IMF cannot be excluded.
This result is not in contrast with the recent findings in Shetty & Cappellari (2014), who find a Salpeter IMF in \( z \sim 0.75 \) massive galaxies. We have also shown (fixing the DM fraction) how the trends of \( M_{\text{dyn}}/M_\star \) could be interpreted within the context of a non-universal IMF, pointing to a varying IMF in terms of the galaxy properties (Tortora et al. 2013, 2014a,c). If we assume a constant DM fraction with redshift, then the observed change of \( M_{\text{dyn}}/M_\star \) is driven by an evolution of the IMF (panels g and h of Fig. 3). IMF is found to vary from a Chabrier or Salpeter IMF at \( z \sim 0.65 \) to a super-Salpeter or very steep IMF at low redshift. However, it is difficult to explain this evolution within the galaxy formation scenario, and in particular through galaxy mergers, since the combination of a ‘higher’ (e.g., bottom-heavier) and a ‘lower mass’ (e.g., bottom-lighter) IMF would produce a dilution in the IMF shape, i.e., this process will not produce a more bottom-heavy IMF, but an intermediate IMF slope. The mergers would decrease \( \theta_{\text{IMF}} \) or leave it almost constant with redshift, as predicted by the galaxy merging toy-models in Sonnenfeld et al. (2017), contrasting the evolution seen in Fig. 3 and suggesting that \( f_{\text{DM}} \) need to evolve with cosmic time. However, a detailed analysis of the joint IMF and DM fraction evolution across the time is beyond the scope of this paper. We will address this issue in future, assuming more complex mass modelling (Tortora et al. 2013, 2014a,c).

Finally, to have a more conclusive answer about the physical processes leading the evolution of these massive galaxies, we have studied how \( R_\star/\Sigma_c \) and \( M_{\text{dyn}}/M_\star \) correlations change with redshift. And we have used toy-models to investigate how this evolution can be explained by the mass accretion from minor- and major-mergings (Boylan-Kolchin et al. 2005; Hilz et al. 2013; Tortora et al. 2014b). We find that our results point to minor mergers as main driver of the mass accretion, since major mergers would produce a too strong mass accretion, which is not observed (Fig. 4, the size evolution is parallel to the \( R_\star/\Sigma_c \) relation for galaxies at the same redshift). To consistently reproduce the evolution in both the size and \( M_{\text{dyn}}/M_\star \), then, we have demonstrated that the accretion of total DM mass would be weaker than the stellar mass one. This can be achieved if the main galaxy is merging with lower-mass galaxies with a smaller \( M_{\text{dyn}}/M_\star \). This result is consistent with independent studies which find that \( M_{\text{dyn}}/M_\star \) is getting smaller at lower masses, down to the threshold mass of \( \sim 10^{10.5} M_\odot \) translating to a star formation efficiency which is increasing from large and massive galaxies to intermediate-mass galaxies (Benson et al. 2000; Marinoni & Hudson 2002; Napolitano et al. 2005; Mendelbaum et al. 2006; van den Bosch et al. 2007; Conroy & Wechsler 2009; Moster et al. 2010).

In a future work we will perform a more systematic study of the IMF, to investigate if it can be considered universal with cosmic time, or if it is changing as a function of the redshift. Then, we plan to have 10 times more galaxies at the end of the KiDS survey, when all the 1500 sq. deg. will have been observed.

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