We measured the coherence properties of the free-electron laser SACLA on a single shot basis at an X-ray energy of 8 keV. By analysing small-angle X-ray scattering speckle patterns from colloidal dispersions we found a degree of transverse coherence of $b_t \approx 0.79 \pm 0.09$. Taking detector properties into account, we developed a simulation model in order to determine the degree of coherence from intensity histograms. Finally we calculated a coherence time of $t_c \approx 0.1$ fs and a pulse duration of 5.2 fs which corresponds with previous predictions.

The rise of X-ray free electron lasers (XFEL) allows the study of physical and chemical properties that could not be accessed experimentally before. In particular, the ultrashort pulse duration on the order of 10 fs at hard x-ray wavelengths of around 1.5 Å offers the possibility to access physical and chemical processes on molecular time and length scales by single shot x-ray diffraction patterns. Many of such studies rely on the coherence properties of the X-ray beam. This includes, e.g., the study of dynamic properties via X-ray photon correlation spectroscopy, imaging single particles and biological specimens by coherent diffractive imaging, cross correlation techniques to reveal a single particle's shape and orientational order in liquids and glasses, or the imaging of ultrafast magnetization processes. XFEL sources such as the Linac Coherent Light Source (LCLS) at SLAC and SACLA at SPring-8 are based on self-amplified spontaneous emission (SASE). The SASE process originates from random fluctuations in the electron beam. Therefore, the coherence properties of such an X-ray source differ from optical lasers. In particular, every single X-ray shot is expected to show certain random features because of the stochastic nature of the SASE process. This was observed recently in experiments at the LCLS and in simulations on the longitudinal coherence properties, where a significant shot-to-shot variation has been observed. In contrast, a SASE beam is expected to show a superior transverse coherence.

Recently, several studies have been performed on the different FEL sources' coherence properties. In the soft x-ray regime, pinhole and double slit experiments have been performed at FLASH and LCLS in order to study the coherence lengths and times. In further studies, interferometry methods have been used to determine longitudinal and transverse coherence lengths. In contrast, coherence properties in the range of hard X-ray have been examined by analysing coherent diffraction patterns, so-called speckle patterns, from disordered samples on a shot-to-shot basis. A similar study has been performed at FLASH. In this study, the degree of coherence is obtained from the speckle contrast. By analysing single shot diffraction patterns from colloidal particles in small angle X-ray scattering (SAXS) geometry, the degree of transverse coherence was found to be almost 1. Furthermore, the longitudinal coherence was determined by wide angle scattering (WAXS) experiments on amorphous metals and it also appeared to be very sensitive on the SASE fluctuations.

Here we present a study of the coherence properties of the free-electron laser SACLA in the hard X-ray regime. In contrast to the LCLS, three bunch compressors and short-period in-vacuum undulators are used at SACLA that result in a compact design compared to LCLS. Furthermore, initial experiments reported pulse durations well below 10 fs. The question arises if and how this design combined with the short pulse duration have an
impact on the coherence properties of the single x-ray pulses. We calculated the degree of coherence for single shots from speckle patterns of colloidal particles at a hard X-ray energy of 8 keV. The number of transverse modes was determined by the need of correcting for the energy bandwidth of the x-ray pulses. The results are supported by simulations of the impact of the charge sharing process of CCD detectors on intensity histograms of speckle patterns. Finally, we estimate the pulse duration from the intensity fluctuations of the beam and compare it to the expected values in the order of 5 fs.

Results

A typical speckle pattern from an amorphous sample together with the azimuthally averaged intensity $I(q)$ is shown in Fig. 1. The experimental speckle size can be determined by calculating the spatial intensity correlation function $g(R) = \langle I(r + R)I(r) \rangle / \langle I(r) \rangle^2$, that is connected to the coherence properties of the beam via the mutual coherence function $\gamma(R, \tau)$ by $g(R) = \vert \gamma(R, \tau = 0) \vert^2 + 1$ at the spatial distance $R$ and time difference $\tau$. $\gamma(R, \tau)$ is a complex function that contains all information of the coherence properties. The degree of coherence for a single speckle pattern is given by $c = \vert \gamma(R = 0, \tau = 0) \vert = 1 / \sqrt{M}$, with $M$ denoting the mode number of the beam. By modelling $g(R)$ with a Lorentzian function for both the vertical and horizontal directions, we obtain a beam size of $(1.9 \pm 0.1) \times (1.6 \pm 0.1) \mu m^2$ which corresponds with the directly measured beam size of $1.8 \times 1.5 \mu m^2$ excellently.

By analysing the speckle pattern the most direct quantity that can be accessed is the speckle contrast or visibility $\beta_s$. It is given by the normalized standard deviation of the intensity yielding

$$\beta_s = \sqrt{\langle I^2 \rangle - \langle I \rangle^2} / \langle I \rangle = 1 / \sqrt{M}.$$ (1)

Due to the equality $\vert \gamma(R = 0, \tau = 0) \vert = 1 / \sqrt{M}$, the speckle contrast directly reflects the degree of coherence of the x-ray beam. A fully coherent beam would have a mode number of $M = 1$ and thus a contrast of $\beta_s = 1$. The experimentally measured contrast is affected by both the longitudinal and transverse coherence of the x-ray beam yielding $\beta_s = \beta_l \beta_t(q)$, with the transverse coherence $\beta_t$ and a $q$-dependent correction $\beta_l(q)$ that depends on the energy bandwidth and the scattering geometry.

In Fig. 2 (a) the contrast $\beta_s$ is shown for 2000 single shots at $q = 0.041 \pm 0.001 \text{ nm}^{-1}$. The average scattering intensity in this $q$-range was 35 photons/pixel. We find an averaged contrast of $\langle \beta_s \rangle = 0.70 \pm 0.08$ which can be taken from the histogram of the contrast values as shown in Fig. 2 (b). This corresponds to a mode number of $M = 2.0 \pm 0.5$. The single shot contrast varies from slightly above 0.5 up to some fully coherent shots with contrast values of 1 following an

![Figure 1](image1.png)
Figure 1  |  (a) Single shot speckle pattern and corresponding $I(q)$ averaged over 500 shots (inset). (b) Typical intensity autocorrelation $g(R)$ and Lorentzian fit to determine the speckle size. Due to the finite size of the extracted region of interest no full decorrelation ($g(R) - 1 = 0$) can be observed.

![Figure 2](image2.png)
Figure 2  |  (a) Single shot speckle contrast $\beta_s$ from 2000 consecutive shots calculated at $q = 0.041 \text{ nm}^{-1}$. (b) Histogram of $\beta_s$. The solid line represents a lognormal distribution using a mean value of 0.7 and a width of 0.105. (c) Speckle contrast $\beta_s$ as function of $q$ averaged over 2000 consecutive single shots. The error bars represent the standard deviation of the single shot values from the averaged value.
asymmetric distribution. This is demonstrated by the solid line in Fig. 2 (b) reflecting a lognormal distribution. In addition, we did not find any significant variation as a function of $q$, see Fig. 2 (c). Taking into account the natural bandwidth of the FEL radiation of $\Delta \lambda / \lambda = 5 	imes 10^{-5}$, the correction accounting for the effect of the longitudinal coherence can be calculated to

$$\beta_i^2 = \frac{2}{L^2 W^2} \int_0^L dx (L - x) \int_0^W dy (W - y) \left[ \exp \left( -2 |Ax + By| \right) + \exp \left( -2 |Ax + By| \right) \right],$$

with beam size $L$, sample thickness $W$, and the coefficients $A = \frac{\Delta \lambda}{\lambda} \sqrt{1 - \frac{q^2}{4k_0^2}}$, $B = -\frac{\Delta \lambda}{\lambda} \frac{q^2}{2k_0}$, and $k_0 = 2\pi/\lambda$. For the $q$-range studied here, we find a correction factor of $\beta_1 = 0.89$, i.e. the transverse coherence is found to be $\beta_t = \beta_i / \beta_1 = 0.79 \pm 0.09$. This corresponds to a transverse mode number of $M_t = 1.6 \pm 0.4$.

Typically, a certain minimum intensity is necessary for contrast calculation using Eq. 1. At low scattering intensities the contrast is usually obtained by describing the intensity distribution by intensity probability distribution functions$^{2,20,23}$. This method was shown to sufficiently describe the contrast of low-intensity speckle patterns in particular at large $q$-range and by using split-and-delay devices$^{27}$. Due to charge sharing of neighboring pixels in the CCD detector and read out noise a continuous histogram is measured with peaks at intensity values corresponding to multiples of single photon events rather than discrete photon events. Typically, experimental intensity values are discretized by rounding up or down to integer values. This may introduce some artifacts. As the ratio of single, double, triple, … photon events is crucial for obtaining the mode number$^{13}$, the interpretation can have a strong impact on the resulting contrast. At low intensities, such problems can be avoided by using so-called droplet algorithms to identify the location of the photons impacting the pixels of the detector$^{3}$. However, those algorithms are limited to very low intensities, in particular, work best for non-overlapping single photon events$^{26}$.

Therefore, here we use the experimental, non-discretized intensity histograms and model those by simulations of intensity patterns following a negative binomial distribution and take into account charge sharing effects of the CCD detector$^{29,30}$ and detector noise, see Methods for details. We used $M = 2$, which corresponds to the experimental value discussed above, as input parameter for the mode numbers. The results are shown as red line in Fig. 3. For comparison, the black circles represent the discrete values before blurring. In particular, at low intensities the results correspond to the experimental data. At higher intensities (see Fig. 3 (b)), the model describes the general shape of the experimentally obtained histogram very well, however, small differences can be found for $I \leq 0.5$ and also at higher intensities. We think this is due to the simplicity of our model and due to a better statistic in the simulation model. Because of blurring, real scattering intensities can appear as lower intensities. For example, a single event of intensity $I_0$ hitting the CCD sensor in between two pixels, will appear as two independent events of intensity $I_0/2$. These can not be distinguished from other events of intensity $I_0/2$ in the same pixels. As a result, experimentally obtained mode numbers from intensity histograms may be overestimated.

Finally we want to discuss the impact of the shot-to-shot intensity distribution. Thanks to the energy bandwidth of $40 \, \text{eV}$, we estimate the coherence time $\tau_c = \frac{\gamma c}{\gamma} = 0.1 \, \text{fs}$, with the speed of light $c$. The coherence time is proportional to the average x-ray pulse duration ($t_p$) via $t_p = M_t \tau_c$, with the average number of temporal modes $M_t$. We determined $M_t$ from the shot-to-shot intensity distribution via a Gamma-distribution$^{11,23}$

$$p_r(I) = \frac{M_t^m}{\Gamma(M_t)} \left( \frac{I}{t_p} \right)^{M_t-1} \exp \left( -M_t \frac{I}{t_p} \right).$$

Discussion

In conclusion, we present a study on the coherence properties of the hard x-ray free-electron laser SACLA based on the analysis of single shot speckle patterns from colloidal particles. The size of the speckles in horizontal and vertical directions are in perfect agreement with expected values. We found a degree of transverse coherence of $0.79 \pm 0.09$ corresponding to a mode number of $M = 1.6$. The degree of transverse coherence is affected by set-up and machine parameters such as bunch compression schemes, saturation length, and photon wavelength resulting in observed values below 1. This is in agreement with expectations from FEL theory$^{12,31}$ and previous experiments$^{6,19,20}$.

By using a simple simulation model, we were able to model experimental intensity histograms. Because of the model’s simplicity, the illustration of the values in the histogram is vague, i.e. they are blurring. This blurring’s origin is related to the charge sharing and the noise level which is present in CCD detectors used in modern x-ray scattering experiments. Such simulation methods will help to determine contrasts more efficiently, in particular for weak scattering.
The sample capillaries were filled into a quartz capillary (diameter of about 0.7 mm) which has been sealed by melting the glass. They had a mean radius of 41 nm with a polydispersity of 10% which was determined over 500 pixels and noise was estimated by computer simulations. Therefore, we used several histograms are scaled for the ADU (Analog-Digital Unit) value for 1 photon of $I(1)$ photons = 124.7 adu. By comparing the simulated histogram with the averaged experimental one we find $\sigma = 0.15$ for the strength of charge sharing and a width of Gaussian noise of $\sigma_{\text{noise}} = 0.1$ photons. The effect of charge sharing is only slightly above the expected value for the MPCCD detector of $\sigma_{\text{MPCCD}} \leq 0.1$ pixels.  

**Methods**

**Sample.** We synthesized the silica colloidial particles by using a modified Stöber method\(^{14}\). The particles were dispersed in water at a volume fraction of about 5%. They had a mean radius of 41 nm with a polydispersity of 10% which was determined by a form factor analysis (see following section). After the preparation the dispersion was filled into a quartz capillary (diameter of about 0.7 mm) which has been sealed by melting the glass.

**Experiment.** The experiment was performed at SACLA’s EH3 of BL3 at a photon energy of 8 keV. With a bandwidth of $5 \times 10^{-4}$ at a repetition rate of 20 Hz\(^{2}\), the pulse energy was (300 ± 40) μJ. The beam was fociwzed with KB mirrors to a size of $1.8 \times 1.5$ μm$^2$ (h × v) at the sample position. The beam size was measured in the vertical and horizontal directions by knife edge scans. The sample capillaries were placed into a holder that was mounted in the MAXIC sample chamber of BL3\(^{2}\). To resolve the structure factor of the samples, the detector (dual multiport charge coupled device (MPCCD))\(^1\), i.e. two sensors with 1024 x 512 pixels each with individual pixel size of 50 μm x 50 μm was placed at a distance of 3 m behind the sample. The accessible $q$-range was limited by the beam stop and the size of the detector to 0.02 nm$^{-1} < q < 0.34$ nm$^{-1}$. For each sample at least 10000 single shot speckle patterns were taken. These were averaged and azimuthally integrated to obtain $I(q)$ as shown in Fig. 1. We measured several 10000 speckle patterns from a diluted dispersion (volume fraction $\leq 0.1\%$) in order to extract the particle form factor. This was fitted by a form factor of a sphere convoluted with a size distribution to account for the polydispersity\(^{15}\). At the volume fraction of 5% used for the correlation analysis a structure factor reflecting particle-particle correlations was visible\(^{15}\), see Fig. 1.

**Charge sharing simulations.** Depending on the detector used, the photons impinging on the CDD sensor generate a charge cloud of different sizes, typically in the order of 10 μm\(^2\). This may result in shortcomings, e.g. an intensity of 1.4 can either be achieved by one photon with negligible charge sharing and less charge sharing contribution from neighbouring pixels, or e.g. by two photons (or more) with non-negligible charge sharing contribution. The impact of charge sharing of the CDD pixels and noise was estimated by computer simulations. Therefore, we used several 500 x 500 pixel grids with values corresponding a negative binomial distribution at an average intensity of 0.36 and 1.54 photons per pixel (identical to the experimental data), respectively. The negative binomial distribution function $p_B(x)$ is given by

$$ p_B(x) = \frac{\Gamma(I + M)}{\Gamma(I) \Gamma(M)} \left( \frac{M}{I} \right)^I \left( 1 - \frac{M}{I} \right)^{-M} x^I e^{-\frac{Mi}{I}}, $$

where $I$ is the intensity in number of photons, $I$ its average, and $\Gamma$ the Gamma function. The initial mode number was set to $M = 2$, matching the result discussed above. Each pixel pattern was blurred by a random Gaussian distribution to model the charge sharing of pixels given by

$$ g(x,y) = \frac{1}{2 \pi \sigma^2} \exp \left( -\frac{(x-x_0)^2 + (y-y_0)^2}{2\sigma^2} \right). $$

Here, $x, y$ denote the pixel coordinate and $x_0, y_0$ the random center of the Gaussian. After that, Gaussian noise was added to the pattern. The amplitude of the charge sharing parameter $\sigma$ and the noise were adapted to match the experimentally obtained histograms. Therefore, we calculated an average histogram from 600 single shots showing low intensities at $q = 0.071 \pm 0.003$ nm$^{-1}$, see Fig. 3 (a). The intensities in histograms are scaled for the ADU (Analog-Digital Unit) value for 1 photon of $I(1)$ photon = 124.7 adu. By comparing the simulated histogram with the averaged experimental one we find $\sigma = 0.15$ for the strength of charge sharing and a width of Gaussian noise of $\sigma_{\text{noise}} = 0.1$ photons. The effect of charge sharing is only slightly above the expected value for the MPCCD detector of $\sigma_{\text{MPCCD}} \leq 0.1$ pixels.  

1. Grubel, G., Stephenson, G. B., Gutt, C., Sinn, H. & Tschatzsch, T. XPCS at the European X-ray free electron laser facility. Nucl. Instrum. Methods 262, 357–367 (2007).
2. Gutt, C. et al. Measuring temporal speckle correlations at ultrafast x-ray sources. Opt. Exp. 17, 55–61 (2009).
3. Hruszkewycz, S. O. et al. High Contrast X-ray Speckle from Atomic-Scale Order in Liquids and Glasses. Phys. Rev. Lett. 109, 185502 (2012).
4. Chapman, H. N. & et al. Femtosecond diffractive imaging with a soft-X-ray free-electron laser. Nature Phys. 2, 839–843 (2006).
5. Seibert, M. M. et al. Single mimivirus particles intercepted and imaged with an X-ray laser. Nature 470, 78–86 (2011).
6. Starodub, D. et al. Single-particle structure determination by correlations of snapshot X-ray diffraction patterns. Nat. Commun. 3, 1276 (2012).
7. Wochner, P. et al. X-ray cross correlation analysis uncovers hidden local symmetries in disordered matter. Proc. Natl. Acad. Sci. 106, 11511–11514 (2009).
8. Wang, T. et al. Femtosecond Single-Shot Imaging of Nanoscale Ferromagnetic Order in Co/Pd Multilayers Using Resonant X-Ray Holography. Phys. Rev. Lett. 108, 237202 (2012).
9. Emma, P. et al. First lasing and operation of an ångström-wavelength free-electron laser. Nature Photon. 4, 641–647 (2010).
10. Ishikawa, T. et al. A compact X-ray free-electron laser emitting in the sub-ångström region. Nature Photon. 6, 540–544 (2012).
11. Saldin, E. L., Schneidmiller, E. A. & Yurkov, M. V. The Physics of Free Electron Lasers (Springer-Verlag, Berlin, 2000).
12. Saldin, E. L., Schneidmiller, E. A. & Yurkov, M. V. Statistical and coherence properties of radiation from x-ray free-electron lasers. New J. Phys. 12, 035010 (2010).
13. Lee, S. et al. Single shot speckle and coherence analysis of the hard X-ray free electron lasers LCLS. Opt. Exp. 21, 24647–24664 (2013).
14. Singer, A. et al. Transverse Coherence Properties of the Free-Electron-Laser FLASH at DESY. Phys. Rev. Lett. 101, 254801 (2008).
15. Singer, A. et al. Spatial and temporal coherence properties of single free-electron laser pulses. Opt. Express 20, 17480–17495 (2012).
16. Varvantyants, I. A. et al. Coherence Properties of Individual Femtosecond Pulses of an X-ray Free-Electron Laser. Phys. Rev. Lett. 107, 144801 (2011).
17. Schlotter, W. F. et al. Femtosecond diffractive imaging with a soft-X-ray free-electron laser. Phys. Rev. Lett. 111, 034802 (2013).
18. Singer, A. et al. Hanbury Brown-Twiss Interferometry at a Free-Electron-Laser. Phys. Rev. Lett. 111, 034802 (2013).
19. Gutt, C. et al. Single Shot Spatial and Temporal Coherence Properties of the SLAC LINAC Coherent Light Source in the Hard X-ray Regime. Phys. Rev. Lett. 108, 024801 (2012).
20. Mai, D. D. et al. Single pulse coherence measurements in the water window at the free-electron laser FLASH. Opt. Exp. 21, 13005–13017 (2013).
21. Inubushi, Y. et al. Determination of the Pulse Duration of an X-ray Free Electron Laser Using Highly Resolved Single-Shot Spectra. Phys. Rev. Lett. 109, 144801 (2012).
22. Nugent, K. A. Coherent methods in the X-ray sciences. Advances in Physics 59, 1 (2010).
23. Goodman, J. W. Speckle Phenomena in Optics (Roberts and Company, Greenwood Village, 2007).
24. Dixon, P. K. & Durian, D. J. Speckle Visibility Spectroscopy and Variable Granular Fluidization. Phys. Rev. Lett. 90, 184302 (2003).
25. Sutton, M. http://www.physics.mcgill.ca/mark/coherence/vorich/highbeta.pdf (2007), date of access:25/03/2014.
26. Abernathy, D. L. et al. Small-Angle X-ray Scattering Using Coherent Undulator Radiation at the ERSF. J. Synch. Rad. 5, 37–47 (1998).
Acknowledgments
We thank the Hamburg Centre for Ultrafast Imaging (CUI) for financial support. The Linac Coherent Light Source (LCLS) at SLAC National Accelerator Laboratory, is an Office of Science User Facility operated for the U.S. Department of Energy Office of Science by Stanford University. The XFEL experiments were performed at the BL3 of SACLA with the approval of the Japan Synchrotron Radiation Research Institute (JASRI) (Proposal No. 2013A8010).

Author contributions
F.L., C.G., W.R., M.Y., T.I. and G.G. designed research. T.K., K.T. and M.Y. prepared the experimental setup. B.F. synthesized and prepared the samples. F.L., C.G., B.F., M.A.S., M.S., S.S., J.G., M.C., S.N., K.T., T.K., A.R. and G.G. performed the experiment. F.L., C.G., W.R. and G.G. analyzed and modeled the data. F.L. and C.G. wrote the manuscript text. All authors reviewed and discussed the manuscript.

Additional information
Competing financial interests: The authors declare no competing financial interests.

How to cite this article: Lehmkuhler, F. et al. Single shot coherence properties of the free-electron laser sacla in the hard x-ray regime. Sci. Rep. 4, 5234; DOI:10.1038/srep05234 (2014).

This work is licensed under a Creative Commons Attribution-NonCommercial-NoDerivs 4.0 International License. The images or other third party material in this article are included in the article’s Creative Commons license, unless indicated otherwise in the credit line; if the material is not included under the Creative Commons license, users will need to obtain permission from the license holder in order to reproduce the material. To view a copy of this license, visit http://creativecommons.org/licenses/by-nc-nd/4.0/
ERRATUM: Single Shot Coherence Properties of the Free-Electron Laser SACLA in the Hard X-ray Regime

Felix Lehmkuhler, Christian Gutt, Birgit Fischer, Martin A. Schroer, Marcin Sikorski, Sanghoon Song, Wojciech Roseker, James Glownia, Mathieu Chollet, Silke Nelson, Kensuke Tono, Tetsuo Katayama, Makina Yabashi, Tetsuya Ishikawa, Aymeric Robert & Gerhard Gruebel

This Article contains an error in the ‘Results’ section. Equation (1)

\[ \beta_s \approx \frac{\sqrt{(I^2) - (I)^2}}{(I)} = \frac{1}{\sqrt{M}}. \]

should read

\[ \beta_s = \frac{\sqrt{(I^2) - (I)^2}}{(I)} = 1/\sqrt{M}. \]