Spin wave damping in periodic and quasiperiodic magnonic structures

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Abstract

We investigated the lifetime of spin wave (SW) eigenmodes in periodic and quasiperiodic sequences of Py and Co wires. These materials differ significantly in damping coefficients, therefore, the spatial distribution of the mode’s amplitude within the structure is important for the lifetime of collective SW excitations. Modes of the lower frequencies prefer to concentrate in Py wires, because of the lower ferromagnetic resonance (FMR) frequency for this material. This inhomogeneous distribution of amplitude of modes (with lower amplitude in material of higher damping and with higher amplitude in material of lower damping) is preferable for extending the lifetime of the collective excitations beyond the volume average of lifetimes for solid materials. We established the relation between the profile of the mode and its lifetime for periodic and quasiperiodic structures. We also performed comparative studies in order to find the differences resulting from complexity of the structure and enhancement of localization in the quasiperiodic system on the lifetime of SWs.

Keywords: magnonics, spin waves, damping, quasiperiodic structures, magnonic crystals

(Some figures may appear in colour only in the online journal)
damping parameter, because it can be directly obtained from the numerical solution in the frequency domain. The lifetime describes the characteristic time of the exponential decay of the amplitude of the mode. This parameter can be related to the linewidth in experimentally measured SW spectra (in ferromagnetic resonance (FMR), time resolved magneto-optical Kerr effect microscope (TR-MOKE) or Brillouin light scattering measurements (BLS)), therefore, we will use the lifetime to describe the influence of damping on collective SW dynamics in inhomogeneous magnetic nanostructures.

The experimental results for inhomogeneous (i.e. nanostructured) systems show the significant dependence of the linewidth on the mode profiles [15, 16]. The lifetime depends on the damping torque, which varies spatially both with the local value of the damping parameter and with the amplitude of SW precession at the given position. The latter dependence can be explained by analyzing the damping term in the LLE, where the strength of damping torque increases with increase of the angle between the effective magnetic field and precessing magnetization vector. It is due to the presence of the cross-product \( \mathbf{M} \times \mathbf{H}_{\text{eff}} \). Thus the modes which will have the amplitudes concentrated in the parts of the systems which are characterized by a lower damping parameter, will be damped to a smaller extent than the modes which are distributed more homogeneously. As a result, the effective lifetime (or damping parameter) cannot be calculated as a volume average of lifetimes (or damping parameters) of the constituent materials. This limitation is even valid for the fundamental mode which also exhibits spatial deviation of the amplitude in different constituents due to different saturation magnetization, partial pinning and the presence of the demagnetizing fields.

In this paper we will establish the relation between the lifetime of SWs eigenmodes and their spatial distribution in magnonic structure, composed of two different ferromagnetic materials, differing also in damping. We will consider planar magnonic crystals (MCs) and quasicrystals (MQs) made of permalloy (Py) (low-damped material) and Co (high-damped material) wires [17–19]. Numerical calculations with the finite element method (FEM) in the frequency domain will be performed for two sets of planar geometries differing in the ratio between the in-plane dimension (width of wires, period) and out-of-plane dimension (thickness). A comparison between periodic and quasiperiodic systems will be presented to analyze the impact of the two effects which enable us to distinguish the quasiperiodic from the periodic system: presence of a complex band spectrum and localization of bulk modes. We will discuss the change of lifetime within the magnonic bands and the global change of this parameter between different bands with the increase of frequency, starting from the metamaterial limit, through the frequency regions, where the concentration in Py subsystems is observed, to a higher frequency range, where the modes start to concentrate in Co wires.

The paper is organized as follows. After the introduction we will discuss: the geometry of the investigated systems, the model, the numerical techniques and tools used to find the frequency spectrum and the profiles of modes. Then we will present and discuss the results—the dependences of lifetime and concentration factor (CF) in Py on frequency. These dependences will be explained with the aid of plots presenting the profiles of modes. The paper will be summarized in a separate concluding section.

2. Model and structures

We considered planar structures composed of ferromagnetic wires arranged in periodic or Fibonacci (i.e. quasiperiodic) sequences—see figure 1. The wires were made of Py and Co—metallic ferromagnets characterized by lower and higher damping, respectively. Both types of wires have the same dimensions. We investigated two regimes of sizes, both for periodic and quasiperiodic sequences, where the widths of wires (along the x-axis) were equal to 91 or 250 nm. The thickness of wires (along the y-axis) was the same for all systems considered by us (30 nm) and their length (along the z-axis) was assumed to be infinite. The wires were in direct contact which ensured exchange coupling between successive wires.

The quasiperiodic sequence of wires was achieved from the following Fibonacci recursion rule [20]: \( S_{N+1} = [S_N + S_{N-1}] \), where the initial structures are: \( S_1 \)—single Co stripe and \( S_2 \)—single Py wire. Then, the next structures are constructed according to the indicated rule by merging the two previous structures (putting \( S_N \) on the left and \( S_{N−1} \) on the right to achieve the \( S_{N+1} \) sequence). We followed this recursion procedure to obtain a quasiperiodic (Fibonacci) sequence \( S_{10} \), consisting of 55 wires (of two kinds: Co and Py).
Because of the Fibonacci recursion rule, there will appear two Py wires next to each other within the structure. Although these wires are not separated and form one Py wire of double width, we will still count them as two Py wires.

To refer the results obtained for quasiperiodic structure to outcomes from the periodic structure, we have investigated a section of periodic system composed of 55 Py and Co wires repeated alternately. Such a number of wires is the same as in the considered $S_{10}$ Fibonacci sequence. We also assumed the sizes of the wires to be the same (as for the quasiperiodic structure) which results in the same total width of the sequence. The assumptions about the sizes of the periodic and quasiperiodic structures make the strength of dipolar interactions comparable for both systems.

We assumed that the static magnetic configuration of the considered structures is saturated by the external magnetic field applied in the direction of the wires’ axis. The field for which we have made our calculations was equal to $\mu_0H_0 = 100$ mT. The material parameters of Co and Py were: saturation magnetizations $M_{Co} = 1.445 \times 10^6$ A m$^{-1}$, $M_{Py} = 0.86 \times 10^6$ A m$^{-1}$; exchange constants: $A_{Co} = 3.0 \times 10^{-11}$ J m$^{-1}$, $A_{Py} = 1.3 \times 10^{-11}$ J m$^{-1}$; and Landau damping parameter: $\alpha_{Co} = 0.1$ and $\alpha_{Py} = 0.01$, respectively. The gyromagnetic ratio $\gamma = 176$ GHz T$^{-1}$ was assumed to be the same for Co and Py wires.

To describe magnetization dynamics we have solved the LLE which is the equation of motion for the magnetization vector $M$:

$$\frac{dM}{dt} = \gamma_0\left[M \times H_{\text{eff}} + \frac{\alpha}{M_5} M \times (M \times H_{\text{eff}})\right],$$

(1)

where: $\alpha$ is the damping coefficient, $\mu_0$ is the permeability of the vacuum, $M_5$ is saturation magnetization and $H_{\text{eff}}$ is the effective magnetic field. The first term in the LLE describes precessional motion of the magnetization around the direction of the effective magnetic field and the second term enriches that precession with damping. The effective magnetic field in general can consist of many terms, but in this paper we will consider only the most important components: external magnetic field $H_0$, nonuniform exchange field $H_{\text{ex}}$ and dipolar field $H_d$: $H_{\text{eff}} = H_0 + H_{\text{ex}} + H_d$.

We considered the linear regime of magnetization dynamics where we could clearly discuss the SW motion on the background of the static magnetic configuration in saturation state and investigate the SW eigenmodes in the system characterized by harmonic dynamics in time: $e^{i\omega t}$, where $\omega$ is the angular frequency. The LLE (1) for the magnetization vector $M$ can be linearized in the form of a set of two differential equations for complex amplitudes of dynamical components of magnetization $m_x$ and $m_y$:

$$(i\Omega - \alpha(r)H_0)m_y(r) = -H_0m_x(r)$$

$$-\frac{2}{\mu_0}\left(\alpha(r)\nabla \cdot \frac{A(r)}{M_5(r)} \nabla m_x(r) + \nabla \cdot \frac{A(r)}{M_5(r)} \nabla m_y(r)\right)$$

$$+ M_5(r)\left(\frac{\partial}{\partial x} + \frac{\partial}{\partial y}\right)\varphi(r),$$

(2)

$$\varphi(r) = \frac{\partial m_x(r)}{\partial x} - \frac{\partial m_y(r)}{\partial y}.$$
The lifetime $\tau$ of the SW modes by the relation: $\text{Im}(f) = (2\tau)^{-1}$ [4, 25]. The parameter $\tau$ describes the exponential decay (in time) of the energy carried by SW. Thus, from the numerical solutions (complex eigenfrequencies) we can get information about the lifetime $\tau$ of each eigenmode.

To show how much of SW amplitude is concentrated in Py wires, we have introduced the measure of concentration for each mode, which we call CF for Py. We defined this parameter according to the formula:

$$\text{CF}_{\text{Py}} = \frac{\int_{\text{Py stripes}} |m_\delta|^2 \, ds}{\int_{\text{Py+Co stripes}} |m_\delta|^2 \, ds},$$

where, in the numerator we have integrated the squared amplitude of the in-plane or out-of-plane component of the dynamical magnetization $m_\delta$ in the Py wires (where $\delta$ is $x$ or $y$, accordingly). The CF is normalized by the integral of the same kind calculated for the whole system. The symbol $ds$ in (7) denotes the element of area for an $x$–$y$ cross-section of the structure. Thus the integrals in (7) are 2D. The values of CF equal to 0 and 1 describe the mode which is concentrated entirely in Co and in Py, respectively. We will show in the next section that there is a strict correlation between the CF and the lifetime of the SWs in MCs and MQs.

It is worth noting that in the considered range of frequencies the modes are almost homogeneous through the thickness of the structure [26] and 1D integration (i.e. along the $x$-direction) could be used in equation (7) as a good approximation. The modes start to be quantized through the thickness at higher frequencies than considered in this paper.

3. Results and discussion

We will discuss separately the outcomes for the systems composed of narrower ($w = 91$ nm) and wider ($w = 250$ nm) wires. The results for the structures with narrower wires are presented in figures 2(a)–(d) where the lifetime and CF for successive eigenmodes dependent on frequency are showed. The gray and green points forming the horizontal lines in figures 2(a) and (b) are the lifetimes for homogeneous films of Py and Co, respectively. Dark blue, light blue and violet points which can be found in the gaps show the lifetime and CF of selected surface modes. Red, orange and brown points show the lifetime and CF of the rest of the modes (mostly bulk modes) found for the Fibonacci and periodic structures. The dashed horizontal lines mark the lifetime of the homogeneous stripe of averaged material parameters.
is not inherited by nanostructures, where the dependence of the lifetime on frequency is observed. The red and dark blue points in figures 2(a) and (b), representing lifetimes of the modes in nanopatterned films, are located between levels denoting the lifetimes of homogeneous films. They show evident dependence on the frequency with two interesting trends: (i) global—the lifetime is relatively short at lowest frequencies (in the metamaterial limit), then increases with increasing frequency, reaches a maximum at about 18 GHz, and decays with the further increase of the frequency; (ii) local—within each magnonic band (gaps between bands are marked by vertical gray stripes) the lifetime increases monotonically with frequency, reaching the highest (the lowest) value at the top (at the bottom) of the band. These trends are common for both periodic and quasiperiodic structures. There is one important difference between the frequency spectra of both structures. The spectrum consists of a finite number of gaps and well-defined bands for the periodic system (figures 2(b) and (d)) and is determined by a complex set of gaps for the quasiperiodic system (figures 2(a) and (c)) [17]. Due to the complexity of the quasiperiodic structure we observe a fractal spectrum [17] with a lot of fine gaps and magnonic states between them. In the considered periodic structure the first magnonic gap appears in the frequency range 16.5–19 GHz, while in MQ the relatively wide gap starts at 14.5 GHz. For the quasiperiodic system more modes have a lifetime closer to the maximum value, than for MC. We also noticed that, for the Fibonacci structure, the lowest modes have got slightly longer lifetimes than modes found in the periodic structure. It results from the different average composition of periodic and quasiperiodic structures built from Co and Py wires of the same dimensions. For the periodic system the filling proportion of Py is equal to 50% (neglecting the ambiguities related to the selection of the first and the last wires in the sequence), while in the Fibonacci structure this parameter is more or less equal to the golden number, which is approximately equal to 61.8%. This suggests that the lifetime for the quasiperiodic system in a metamaterial (long wavelength) regime should be larger and closer to the value characteristic for the solid Py film than for the periodic system. The lifetimes calculated numerically for homogeneous systems made of averaged material parameters—$A$, $M_5$ and $\alpha$ (with volume fraction of Py at 50% like in the periodic structure and 61.8% like in the quasiperiodic one)—confirm this suggestion, but they are noticeably overestimated (0.97 ns and 1.24 ns for the smaller and larger filling fractions, respectively) in relation to the lifetimes of the lowest (i.e. fundamental) mode in MC and MQ, respectively (figures 2(a) and (b)). Thus, there is need to investigate this structurally induced change of damping in a more systematic way with detailed analyses of the distribution of SW amplitude.

To relate the lifetime of the modes with the spatial distribution of their profiles, we plot (in figures 2(c) and (d)) the CFs in the Py system: $C_{F_x}$ and $C_{F_y}$ defined by equation (7) for the components $m_x$ and $m_y$ of dynamical magnetization, respectively. The dependences of $C_{F_x}$ (brown points) and $C_{F_y}$ (orange points) on frequency are qualitatively the same, but differ in the values they reach—$C_{F_y}$ is noticeably bigger than $C_{F_x}$. The difference between CFs for $C_{F_x}$ and $C_{F_y}$ results from the symmetry of the system. Due to differences in $x$- and $y$-components of dynamical dipolar fields, the component $m_x$ is strongly reduced in reference to the $m_y$ component (ellipticity of precession is larger) in Co stripes, relatively to Py stripes.

We expect that modes of higher concentration in Py will be characterized by a longer lifetime than those concentrated in Co. For these modes the damping torque is low in both the Py and Co subsystems. A small damping torque in Py appears because of the low value of intrinsic damping (small $\alpha$), while the reduced damping torque in Co results from the small amplitude of the SW precession (and low value of $M \times H_{eff}$—see equation (1)). Figures 2(c) and (d) present the dependence of $C_{F_y}$ on frequency for periodic and quasiperiodic systems, respectively. Both the global change of the lifetime as a function of frequency and the local changes of this parameter within each band are clearly reflected in the dependence of the CF on frequency. This supports our explanation of nonlocal reduction of damping in Co/Py nanostructures, resulting from different distribution of the amplitude of SWs between Co and Py subsystems. It is worth noting that the relation between CF and lifetime is not linear, which results from a nonlinear relation between precession amplitude and damping torque. CF can also reflect some other peculiarities of mode profiles. All these effects can result in the lack of one-to-one correspondence between the CF and the lifetime. For instance, the ranges of $C_{F_y}$ for the second and the third magnonic bands overlap (see figure 2(d)) but their ranges of corresponding lifetimes are separated—it means that we can have two states of the same $C_{F_y}$, which differ in terms of lifetime. The other problem is some ambiguity in the definition of CF, which is related to the measure used in equation (2)—we choose the most intuitive formulation of CF—we have integrated the squared absolute value of $|m_y|^2$ (and not e.g. the absolute amplitude $|m_y|$). This particular choice affects only quantitatively the dependence of CF on frequency and can be justified by the relation of experimental characteristics to the squared amplitude of SWs. Overall, the calculated CF explains the general change of lifetime dependent on frequency.

For further analysis of the impact of the shape of profiles on the lifetime of SWs, we plotted selected modes from quasi-periodic (figure 3) and periodic sequences (figure 4). We pay attention to the location of the nodes and to the position of the areas of the SWs’ amplitude concentration. We start our discussion from the description of the lowest modes in the frequency scale i.e. in the metamaterial regime. In this frequency range the modes vary in terms of the scale of the whole structure, being relatively smooth across the distances comparable to the sizes of the single elements composing the nanostructure. Thus, the lowest SW modes have very little oscillations and nodes. Their amplitude (in both Py and Co subsystems) goes rarely to zero and follow the long-scale oscillations characteristic for the metamaterial regime (see modes 1, 2, 3 in figures 3 and 4). As a result of relatively high amplitude of SWs also in Co, the lifetimes of the lowest modes are short.

When we look into the details of the profiles of the lowest modes, we see that the amplitude in Co is slightly lowered in comparison to the amplitude in Py. However, this finding does
not undermine the previous conclusion about high damping of the lowest modes. The lowering of the SW amplitude in Co can be easily understood when we notice that the frequencies of these modes are below the FMR frequency of Co. It means that the SW amplitude will decay into the center of Co wires from the forced oscillations at the Py edges (only exponential decay is accepted below the FMR frequency). This slight lowering of the amplitude in the Co subsystem could suggest that the lowest modes will have a longer lifetime in comparison to the modes in a homogeneous system (formed by averaging of the material parameters, including the damping constant), where the amplitude changes smoothly. But, in fact, the opposite is true: the lifetime of fundamental mode for the nanostructure is slightly lower than for the average system. This finding demonstrates that the volume averaging of the damping constant is not a fully justified approach in magnetic composites, even at the long-wavelength limit. The lifetimes of higher modes, starting from the fundamental excitation, grow with frequency because of the increase of the number of nodes which are usually located in Co. This reduces the damping torque in Co and extends the lifetime (see e.g. mode 20 in figure 3 and mode 28 in figure 4).

We will focus now on higher-frequency SWs (from higher bands) in the MC. In the second band (modes 31–56 in figure 4) all modes have one node in every Py wire. This reduces the averaged amplitude in the Py subsystem as compared to the excitations of the first band. As a result of increasing the contribution of SWs excited in Co, the lifetime for SWs in the second band will be shortened. Similar arguments can be used to explain the reduction of the lifetime in the third band (where two nodal lines in each Py wire are observed) in reference to the second one.

The scenario for changes of lifetime within the second band is similar to the first band: while in all Py wires one node is observed, successive modes have more and more Co wires with nodes; this gradually increases the lifetime. We can explain similarly the changes of mode profiles in the third band (modes 59–84), where two nodal lines in each Py wire appear. This led us to the same conclusion about the changes of lifetime within the third magnonic band as for the previous ones.

The presented mechanism seems to be systematic and can be used to explain the increase of the lifetime of the modes within the bands with increasing frequency and reduction of the lifetime of a higher band in reference to a lower one. However, this clear picture is not valid for high-frequency bands, where SWs start to oscillate spatially in Co. The harmonic oscillations in Co stripes appear at higher frequencies, well above the FMR frequency for Co, due to the finite width of the wires. Changes of the spatial distribution of SWs’ amplitudes are much more complex with increasing frequency and are difficult to describe in the frame of a simple mechanism. We will investigate them briefly for wires of larger widths in the last part of this section.

We will now discuss the relation between SWs’ mode profiles above the metamaterial regime frequencies in the
There are two important structural differences in reference to a periodic sequence that are worth stressing. The first difference is that in the considered quasiperiodic structures there are Py wires both of single and of double width. The second difference is lack of periodic repetition of elements in the structure. Due to two different widths of wires the modes can concentrate in both kinds of Py wires. The lower modes (see e.g. modes 23, 34, 35 and 46 in figure 3) are concentrated mostly in wider Py wires, while higher modes start to be excited in the single Py wires (e.g. modes 49 and 84). Thus, the quantization of SWs within Py wires depends also on the width of wires. In single Py wires the increase of the number of nodes (or spatial oscillations) appears with larger differences of frequencies — e.g. modes 49 shown in figure 3) are concentrated mostly in wider Py wires, while higher modes start to be excited in the single Py wires (e.g. modes 49 and 84). Thus, the quantization of SWs within Py wires depends also on the width of wires. In single Py wires the increase of the number of nodes (or spatial oscillations) appears with larger differences of frequencies — e.g. the group of modes with one node (e.g. mode 49 shown in figure 3) and the group with two nodes in Py wires (e.g. mode 84) are more separated in the frequency domain than the group of modes concentrated in double wires (in double Py wires) — e.g. mode 23 in figure 3 originating from the group with one node in double Py wire and mode 35 with two nodal points in double Py wire.

The lack of regular arrangement of elements (sets of wires) in the quasiperiodic structure means that every Py stripe can have a unique surrounding [17]. This strengthens the localization of SWs, due to very few (if any) equivalent locations for SW eigenmodes (see modes with numbers larger than 23 in figure 3). The small number of Py wires with a significant amplitude of modes, protects the distribution of the modes across the whole structure. It is worth noting that an eigenmode in the quasiperiodic structure can be formed by excitation in a few Py wires only if they have a similar surrounding to the other stripes [17].

For the Fibonacci quasiperiodic structure it is not easy to analyze the frequency spectrum, because it is impossible to point out the allowed frequency bands. We can only find its counterpart by the complement of the complex, fractal set of magnonic gaps [17]. For the finite structure the magnonic gaps can be found as frequency ranges of the width much bigger than the average frequency interval between successive modes. However, this limits the detection of the fine magnonic gaps, therefore, in figures 2(a) and (c) we identified only the widest magnonic gaps in the spectrum.

In the case of MQs, the systematic discussion of the changes of mode profiles and their lifetimes is difficult to pursue in the manner presented for the MC. We selected for discussion only some modes at the edges of the largest magnonic gaps (modes

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**Figure 5.** (a) and (b) Lifetime of SW eigenmodes versus their frequencies for (a) Fibonacci structure—MQ and (b) periodic structure—MC, consisting of 55 wires of 250 nm width. (c) and (d) The CF for the $m_x$ component (brown and violet points) and $m_y$ component (orange and light blue points) of SW eigenmodes showing the strength of the excitation within the Py subsystem for (c) MQ and (d) MC. The grey areas mark the most pronounced frequency gaps. The green (grey) horizontal series of points show the lifetime of eigenmodes obtained for a solid Co (Py) layer of the same external thickness and width as considered for the MC and MQ structures. The dashed vertical green and grey lines mark the frequency of the first FMR mode obtained for the homogeneous Co and Py stripe, respectively. Dark blue, light blue and violet points, which can be found in the gaps, show the lifetime and CF of selected surface modes. Red, orange and brown points show the lifetime and CF of the rest of the modes (mostly bulk modes) found for the Fibonacci and periodic structures. The dashed horizontal lines mark the lifetime of the homogeneous stripe of averaged material parameters.
These modes differ significantly in terms of spatial distribution of SW amplitude, which results in noticeable differences in their lifetime. We found three main features of the profiles of modes in the quasiperiodic system which affect clearly the lifetime of those modes. These are: (i) the ratio of the number of double to single Py wires in which high amplitude of the SW mode is concentrated, (ii) the number of nodes in Co wires (especially in those located next to the Py wires, in which the amplitude concentrates), and (iii) the number of nodes in Py wires. The best composition of the mentioned conditions, which will give us the guidance to pick up the profile of the mode characterized by a long lifetime, is: the mode should be concentrated in the double Py wires with a low number of nodes inside of these wires and should decay rapidly in the surrounding Co wires, which can be ensured by nodes being located in the Co. If we compare e.g. modes 34 and 84, we will be able to explain the differences in the lifetimes of those modes (short lifetime for mode 84 and long lifetime for mode 34) in terms of the discussed features.

The considered systems are finite sequences of elements (wires) ordered in periodic or quasiperiodic manner. For such structures both the bulk states (forming the frequency bands) and surface states (appearing in frequency gaps) can exist. The frequency gaps are the frequency ranges forbidden for the bulk modes. However, surface states, which are localized on the external wires (and exponentially decaying inside of the structure), can exist in these frequency ranges. For the structures under consideration, the external stripes are made of Py (for both periodic and quasiperiodic structures), therefore, most of the amplitude of the surface modes is concentrated in the material of low damping (Py). This explains the relatively long lifetime of these modes (figures 2(a) and (b)). It is worth noting that, due to the significant width of the structure (and big separation between surfaces), two surface modes appearing in one gap are practically degenerate and their lifetimes are practically the same, although in the quasicrystal the y-axis of symmetry is not present.

We are going to discuss now the results obtained for the larger structures i.e. for the systems made of wider wires. The dependences of the lifetime and CF for the structures built from wires of 250 nm width were set together in figure 5. We chose to use the style of points, lines and the ranges of frequency and lifetime the same as in figure 2 to make the comparison of the plots presented in figures 2 and 5 easier. Comparing obtained results for the structures made of narrower wires (figure 2) to the results for wider wires (figure 5), it is easy to notice that the lifetime of eigenmodes changes within similar limits in the same frequency ranges. We can make the same observation for dependences of CF on frequency, which is also presented in figures 2 and 5.

The most distinctive difference between the spectra for the systems presented in figures 2 and 5 is a difference in the number of magnonic gaps and bands. It is because of the differences of the widths of wires. For the periodic system the width of wires (and as a result the period) determines the size.
of the first Brillouin zone and location of frequency gaps. The system of wider wires is characterized by a finer frequency spectrum. This rule can be also generalized for quasiperiodic systems. In our study we keep the total number of wires within the structure constant (i.e. equal to 55), therefore, the number of modes per one band is the same for the structures with narrower and wider wires.

The general trend of the dependence of lifetime and CF versus frequency is more or less the same for each of the considered structures: the envelope goes at first up, reaches a maximum at around 18 GHz and then it starts to fall down. This dependence is more dynamic (i.e. has steeper slopes) for structures built from wires of 250 nm width. In the considered range of frequencies we obtain for the periodic sequence of narrower wires (figures 2(b) and (d)) 3 bands and 3 gaps, and for the periodic sequence of wider wires (figures 5(b) and (d)) 8 bands and 8 gaps. For quasiperiodic systems we marked only the widest gaps but the increase of the number (or density in the frequency domain) of magnonic gaps is evident for the structure with wider wires (figures 5(a) and (c)). We noticed that the modes in the structures constructed from wider wires, are on average less damped (have got a slightly longer lifetime) than the modes for systems built with narrower wires.

The profiles of modes for structures with wider wires are presented in figure 6 (for quasiperiodic structure) and in figure 7 (for periodic structure). In general, the profiles of modes for the periodic and quasiperiodic systems look quite similar to those presented in figures 3 and 4. The lowest modes (i.e. the modes in the metamaterial regime) look practically the same as their counterparts in figures 3 and 4. Some differences in the shape of the corresponding modes from the structures differing in the width of wires can be attributed to different frequencies and different relations between dipolar and exchange interactions—compare the last modes in the first band for periodic sequences of narrower wires (mode 28 in figure 4) and wider wires (mode 26 in figure 7).

The important difference between figures 2 and 5 for the systems with narrow and wide wires, respectively, is the presence, in the later system, of the band of modes which are almost entirely concentrated in the Co wires. For the periodic (quasiperiodic) sequence we observe a band of modes nos. 169–195 (210–225), which are highly damped and characterized by lifetimes close to the lifetime of the homogeneous film of Co—see figures 5(a) and (b). The selected profiles are presented in figures 6 and 7.

For each of the considered structures a similar dependence of the lifetime and CF on frequency within the magnonic bands can be found: the modes at the bottom of the band are the most damped and then their damping is gradually reduced with the increase of the frequency. The only exceptions to this
rule are the bands of modes concentrated in Co, where the lifetime of modes is reduced with increasing frequency.

All considered structures are terminated with Py stripes. Due to the low damping of Py, the surface modes (mostly concentrated in the outermost Py stripes) are characterized by relatively long lifetimes.

We also inspected carefully the bottoms of magnonic bands to check how SWs penetrate Co wires, which is the main source of the increase of damping for modes concentrated mostly in Py. We found that for some modes (e.g. mode 29 for the periodic sequence in figure 7) the amplitude of SWs does not decay in the center of Co wires and, therefore, these modes can be considered as modes supporting the SW dynamics in both the Py and Co subsystems.

4. Conclusions

We have showed that SW lifetimes in 1D planar MC and MQ systems differ substantially from damped SWs in planar homogeneous systems. We have investigated nanostructures composed of the two materials: the one characterized by lower saturation magnetization and lower damping and the other one with higher saturation magnetization and higher damping. For such systems the lifetime of eigenmodes can be extended over the lifetime of modes in a homogeneous slab, made of artificial material, characterized by parameters, being the volume average of parameters for Co and Py. The frequency dependence of lifetime for the nanostructure is not constant, as it is for a homogeneous layer in a Damon–Eshbach configuration [25], but shows specific dependence, having common features for periodic and quasi-periodic bandgap materials, and for the two different aspect ratios of the xy-cross-section of Co and Py wires. For the lowest modes the lifetime is slightly below the value of this parameter for the homogeneous layer of averaged material parameters, then increases, and after reaching the maximum, decays gradually. These changes take place in the frequency range corresponding to the lowest magnonic bands, where the modes are concentrated mostly in the low-damped material—Py. For higher frequencies we start to observe (for the structures with 250 nm wide wires) the bands of the modes which are concentrated in Co and characterized by very short lifetimes. Those bands are out of the earlier-described trend.

Our main finding is the description of the relation between spatial distribution of amplitude of the SW eigenmodes and their lifetimes. We were able to correlate the concentration of the mode in a Py (or Co) subsystem (expressed by an introduced measure of this concentration) to its lifetime. We also inspected carefully the bottoms of magnonic bands to check how SWs penetrate Co wires, which is the main source of the increase of damping for modes concentrated mostly in Py. We found that for some modes (e.g. mode 29 for the periodic sequence in figure 7) the amplitude of SWs does not decay in the center of Co wires and, therefore, these modes can be considered as modes supporting the SW dynamics in both the Py and Co subsystems.

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