Pyrolytic carbon: applications of its diamagnetism in metrology

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Abstract. This paper presents some current or potential applications in metrology based on the diamagnetism of pyrolytic carbon (PyC). The magnetic repulsion force acting between a piece of PyC subjected to a magnetic flux can be used as magnetic spring either to control the position of the sensitive sensor element or to detect changes of a physical quantity to be measured. The first part of this paper provides examples briefly described of devices based on the diamagnetism of PyC for measuring mechanical quantities. There are two main configurations for magnetic levitation: one, used for measuring acceleration or inclination for instance, is based on the levitation of a PyC tile above a magnet or set of magnets; In the other, used to measure forces caused for example by contact or buoyancy, it is the permanent magnet that is levitated at a stable height above a fixed PyC tile. The second part describes current work at the Laboratoire Commun de Métrologie (LCM-LNE/CNAM) on the development of new laser power sensors using either diamagnetic force changes by photothermal excitation of electrons or diamagnetic torsion spring.

Keywords: Accelerometer / force meter / laser power / magnetic levitation / pyrolytic carbon / tiltmeter

1 Introduction

An object made from a diamagnetic material is repelled by a magnetic field. As a consequence of Earnshaw’s theorem [1,2], this property can be used to create a local minimum in the potential energy in magnetic fields and stabilize magnetic forces. Note that it took about 160 years from discovery of diamagnetism to the first practical demonstration of levitation [3]. Many natural substances (water, wood, carbon, etc.) or artificial ones (e.g. plastic) are weakly diamagnetic. The elements displaying the strongest diamagnetism at ambient temperature are the naturally occurring element bismuth and the man-made material pyrolytic carbon. In his PhD thesis, Pigot [4] showed how the diamagnetic properties of bismuth and the man-made material pyrolytic carbon. In his PhD thesis, Pigot [4] showed how these two means of levitation: one, used for measuring acceleration or inclination for instance, is based on the levitation of a PyC tile above a magnet or set of magnets; In the other, used to measure forces caused for example by contact or buoyancy, it is the permanent magnet that is levitated at a stable height above a fixed PyC tile. The second part describes current work at the Laboratoire Commun de Métrologie (LCM-LNE/CNAM) on the development of new laser power sensors using either diamagnetic force changes by photothermal excitation of electrons or diamagnetic torsion spring.

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2 Pyrolytic carbon diamagnetism

The PyC diamagnetism anisotropy is characterized by a magnetic susceptibility component \( \chi_x \approx -4.5 \times 10^{-4} \) which greatly exceeds the components \( \chi_y \approx -0.85 \times 10^{-4} \). This strong directional diamagnetism can be used to stabilize, in a magnetic flux density, the free levitation of either a piece of PyC above a permanent magnet or a permanent magnet below a sheet of PyC.

In addition, the different magnetic stiffnesses generating restoring forces can be used for measuring external forces applied in translation along the \( x, y \) or \( z \)-axes or in rotation around the \( z \)-axis.

Figure 1 shows an example of these two means of levitation. Note that stabilized levitation using PyC was
Concerning "patented for the first time [6] in 1971. In this patent concerning “diamagnetic levitation and/or stabilizing devices”, the use of PyC levitation is clearly claimed as follows: "Another object of the invention is to provide diamagnetic levitation and/or stabilizing devices particularly adapted for the use of pyrolytic graphite diamagnetic members in relation to the magnetic fields of permanent magnets".

The three most remarkable advantages of the use of PyC diamagnetism for metrology are:

- first, PyC levitation in contrast to superconducting levitation [7] works at ambient temperature with no need for cryogenics nor indeed any energy input whatsoever if permanent magnets are used.
- secondly, the levitation of either a PyC plate or a permanent magnet as sensitive element means the measurement accuracy is limited neither by friction, nor parameters such as stiffness changes, wear thermal expansion and fatigue.
- thirdly, the low cost and the simple implementation of the base elements (PyC plate and NdFeB magnets) which make it easy to develop a sensor based on PyC diamagnetism (levitation).

The stabilization of the levitation of a piece of PyC depends on the 3D magnetic field. Several authors [8–10] have studied the magnetic field distribution created by different arrangements of permanent magnets.

Since the 1960s, many applications for diamagnetic levitation appear to be promising [11] for sensing (e.g. accelerometers) and linkage devices of extremely low intrinsic friction (e.g. magnetic bearings or micro-rotors).

Note that most of sensors based on PyC diamagnetism presented here are not measurement standards (or etalons) but rather just sensors as defined by the international vocabulary of metrology [12], i.e. "element[s] of a measuring system that are directly affected by a phenomenon, body, or substance carrying a quantity to be measured", for which the physical stimulus can be heat, light, sound, pressure, magnetism, or a particular motion. Often, they have been developed for specific applications with constraints linked to measurement range, transducer design, implemented technology, environmental conditions, etc.

Figure 1. Example of levitation at ambient temperature with no energy supplied: (a) square PyC tile levitated above an array of four cubic NdFeB magnets of side 10 mm. (b) cubic NdFeB magnet of side 5 mm subjected to the attraction of a permanent magnet located above the device (not visible in the photograph) maintained in stabilized levitation between two PyC sheets.

3 Accelerometer

3.1 Principle

Inertial sensors have an internal mass (seismic mass) in a spring system which any external acceleration causes to be displaced. They are used as accelerometers or gyroscopes to measure acceleration along a defined direction.

Micromachined high-resolution vibration sensors or accelerometers include capacitive [13–16], tunneling [17,18], piezoresistive, optical [19], inertial MEMS [20], piezoelectric and ferroelectric sensors. There are also other types of industrial sensors based for instance on piezoresistivity (strain gauges), the (classical) Hall effect, mutual induction or eddy currents.

3.2 Examples of device

Several configurations of inertial sensors based on a PyC tile floating above a permanent magnet array have been designed. Their differences concern mainly the motion detection system.

Barrot et al. [21] have presented a novel force feedback acceleration sensor concept, featuring levitation of the inertial mass. Their device is a low cost 2D or 3D-accelerometer based on diamagnetic levitation and electrostatic actuation. The accuracy of this kind of device depends essentially on the electronics associated with the displacement detection of the PyC element. A PyC disc (28 mm diameter) surrounded by an aluminum ring which floats 250 μm above a horizontal arrangement of permanent magnets constitutes the seismic mass (1.68 g).

Figure 2 shows the schematic diagram of a low-cost accelerometer in the 2D-configuration. The measuring range lies between $10^{-9}$ g and 1 g $(g \approx 9.81 \text{ m s}^{-2} \text{ being the Earth’s gravitational acceleration})$. For instance, the resolution of the 2D acceleration sensor is about $10^{-9} g \approx 10^{-9} \text{ m s}^{-2}$ at 0.5 g. The sampling rate (5 kHz to 10 kHz) used for the position control of the levitated seismic mass is high compared to the frequencies of seismic signal (0.1 Hz to 20 Hz). One of the main potential applications of this sensor is seismic monitoring of civil engineering structures.

More recently, Andò et al. [22,23] have developed an acceleration sensor based on an inductive detection that can operate either in displacement or in acceleration mode. It is a low-cost differential inductive readout device based on an inertial sensor using a levitated PyC tile (1.2 cm$^2$) suspended above four NdFeB magnets. The levitation mechanism allows low friction and high sensitivity.
The sensitivity and the resolution of the sensor are 1.17 V/(m s⁻²) and 10⁻⁴ m s⁻² in acceleration operating mode and 0.61 V/mm and 1.9 × 10⁻⁴ mm in displacement operating mode, respectively. These capabilities can be compared with the limit of in-run bias stability for MEMS accelerometers, which is about 1.5 × 10⁻⁴ m s⁻² in acceleration operating mode, i.e. close to the resolution of PyC-diamagnetism-based accelerometers, thus making the latter very competitive.

4 Tiltmeter

4.1 Principle

Tiltmeters are very sensitive inclinometers used to measure and record small deviations of a horizontal reference platform from orthogonality to the vector of local gravity. Equivalent to long-length stationary pendula, they are used for monitoring small changes on the ground (landslides such as rockfalls, mudflows, deformation of volcanoes, etc.) or in structures such as loading and foundation settlement.

4.2 Example of device

In the literature, we found only one example of an inclination sensor based on PyC levitation namely that described in 1968 by Simon et al. [24]. The tiltmeter is a horizontal pendulum type whose mass consists of a diamagnetic PyC rod suspended in the potential well of magnetic forces that are separated by PyC plates. Three confocal sensors are used to measure the inclination of the permanent magnet in levitation subjected to the applied force to be measured.

Figure 3 shows the schematic diagram of the passive PyC levitation system of the tiltmeter. The tiltmeter was designed for measurement of extremely small tilts of (buoyancy, stiffness, etc.) or dynamically to transfer energy to the system to determine the magnitude of the desired quantity (friction, thermal diffusion, etc.) from the system response.

5 Force sensor and force-based sensor

5.1 Principle

A wide range of techniques is used to measure mechanical micro-forces. Such sensors are usually composed of an elastic structure on which the force being measured acts (cantilevers), and of a deformation or displacement sensor (strain gauge, capacitive, optical or piezoelectric detection, etc.). In addition, a balancing device generating an electrostatic, electromagnetic or piezoelectric force feedback can be added to improve accuracy.

All the sensors presented above use a PyC levitation configuration like that shown in Figure 1a, but in the case of force sensors, most of the examples found in the literature use levitation of a permanent magnet diamagnetically stabilized by pieces of PyC as shown in Figure 1b. Permanent magnets and coils allow one to maintain the permanent magnet in levitation subjected to the applied force to be measured.

There are also force-based sensors where a force is used for measuring other physical quantities. Typically, this force is generated either statically to balance a restoring force induced by the phenomenon, body or substance considered and linked to the quantity to be measured (buoyancy, stiffness, etc.) or dynamically to transfer energy to the system to determine the magnitude of the force to be measured.

There are several difficulties involved in measuring small contact forces and calibrating micro- and nano-force sensors. For measurement, one needs to determine and control the point of application and the alignment of the direction of force (a vector quantity). For calibration, one needs to understand the problems of coupling, interface and contact interaction (adhesion, friction) as well as the unwanted phenomena at the contact surface between the reference standard and the measurement device to be calibrated (sources of error).

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5.2 Examples of application

5.2.1 Contact force sensor

At the FEMTO-ST institute in Besançon (France), Abadie et al. [25] have developed a low frequency micro- and nano-force sensor based on a 10-cm long capillary tube used as levitating seismic mass. The force measurement range varies between ±50 μN and the resolution reached with a confocal chromatic sensor is about 5 nN. Figure 4 shows a schematic diagram of this force sensor using a levitating tube.

Another device has been developed by Cherry et al. [26] at the FEMTO-ST institute. Here, instead of a levitating tube, the seismic mass sensitive to external forces is a floating platform. The platform supports permanent magnets of which the magnetic forces interacting with external permanent magnets are stabilized by means of PyC plates. Three confocal sensors are used to measure the displacements of the platform. The measurement range varies between ±50 μN while the resolution can reach less than 10 nN if an anti-vibration table is used.
In another example, Li et al. [27] have developed a diamagnetic lateral force calibrator composed of four NdFeB magnets and a diamagnetic pyrolytic graphite sheet to calibrate directly an atomic force microscope cantilever-tip or -bead assemblies. This sensor provides both the lateral force and the crosstalk lateral force constants with an accuracy on the order of 0.1%. The spring constant of about 10 pN/nm is measured with 10⁻⁴ relative accuracy and is used for calibrating the AFM lateral constants. The location uncertainty of the shear centre of the cantilever constitutes the main difficulty of the measurement method.

All these devices based on PyC diamagnetic present interesting features. For comparison in terms of resolution, Fahlbush and Fatikow [28] have tested semiconductor strain gauges attached to a microgripper used as a self-sensing cantilever for atomic force microscopes. The resolution is about 2 nN in the range of a few microns. Kim et al. [29] have presented a monolithic MEMS-based microgripper to manipulate biological cells. The device has an integrated force feedback based on capacitive force sensor with a gripping force resolution of about 20 nN in the range of a few tens of micrometrons.

Whatever the case, calibration of small force sensors is particularly complicated and lacks real traceability. However, although the calibration is for the sub-piconewton range, the work of Melcher et al. [30] can be mentioned. The authors have developed an ultrasensitive optomechanical sensor with a stiffness of 4 μN/nm, designed to improve the accuracy and precision of force measurements with atomic force microscopy. Its self-calibration is realized through using the radiation pressure from light incident on the cantilever surface. The force resolution of this device is estimated to be 14 fN in the range from zero to a few hundreds of a femtonewton.

5.2.2 Viscosity and density sensor

Clara et al. [31] have investigated the feasibility of using a “floater” magnet (a permanent magnet in levitation about 0.6 mm above a piece of PyC) immersed in a liquid to measure its density and viscosity. Figure 5 shows the principle of the set-up developed at the Johannes Kepler University in Linz (Austria).

The density of the fluid can be determined by balancing the buoyancy force and the magnetic force acting on the “floater” magnet to keep its levitation height constant in the liquid under test. The “floater” magnet is levitated using a “lifter” magnet (permanent magnet). The height of the “floater” magnet is measured over the vertical magnetic flux density by a Hall effect sensor placed beneath the pyrolytic carbon. The position of the “lifter” magnet is adjusted to keep the height of the “floater” magnet constant. There is a relation between the position of the “lifter” magnet and the buoyancy force which is related to the density of the fluid. This method is applicable for a large range of densities from below 1 kg/m³ (approximately that of air) to 1300 kg/m³ (1.3 times that of water), but the relative error depends on the levitation height. For instance, the relative error in the density measurement lies between 0.1% and 1% for a levitation height of 0.75 mm. The sensitivity of the experimental set-up is about 4 μm/(kg·m⁻³) and the resolution in height measurement is about 0.01 mm.

For viscosity measurements, an AC-driven coil is added to the “lifter” magnet. The AC-component superposes an alternating magnetic force which induces oscillations of the “floater” magnet. The resonance frequency for the set-up is around 6 Hz. The damping of the resonance is related to the viscosity of the fluid. The quality factor falls with increasing dynamic viscosity. The best results are obtained for low viscosities in the range below 20 mPa s. No estimate of measurement uncertainty is provided in the paper.

Note that the accuracy of this device is not very high compared with classical methods used at any National Metrology Institute. For instance, the determination of the density of a liquid by means of the pycnometric method is provided with relative uncertainty of about 0.05% and the relative uncertainty for measurement of dynamic viscosity in the range below 20 mPa s is about 0.5%.

6 Laser power meter

6.1 Photo-thermal excitation

Laser power meters are mainly based on either thermal measurement techniques via the Stefan-Boltzmann law (thermopile sensors) or the photon-electron interaction (photodiode sensors). The LCM/LNE-CNAM is currently
developing three experimental configurations based on a repulsive force acting on a piece of PyC in a magnetic induction generated by a magnet array to measure laser power in an intermediate range from a few hundred of milliwatts to a few watts.

The first two are based on the change of PyC diamagnetism due to photo-thermal excitation of electrons by laser radiation. The third uses 3D-stabilisation of a levitated PyC disc as a passive magnetic spring to detect the radiation pressure of a laser beam. Up to now, most of our experimental measurements have been carried out for the power range 100 mW to 1 W at a wavelength of 1064 nm.

The experimental setup of the first configuration [32] similar to that of Figure 1a is very simple. In this case, the repelling diamagnetic force is modified by the laser beam irradiating with an incidence angle perpendicular to the PyC surface that involves the levitation height change which is measured by means of an optical position sensor with a resolution of 10 nm. There is a quasi-linear relation between the optical power change and the levitation height change. The photo-response sensitivity of this laser power meter is about 100 mW μm⁻¹ and its discrimination threshold is about 3 mW. The main environmental quantities influencing the measurement are temperature and the background noise due to vibrations and movements of air. Its relative uncertainty for optical power measurement between 0.4 and 1 W at 1064 nm is less than 10%. The accuracy of this device is not competitive with that of photodiode or thermopile sensors where the laser power measurement uncertainty is close to 1% just after calibration. Figure 6a shows the photograph of a set-up and Figure 6b gives an example of response in terms of mass after 60 s irradiation at 532 nm for 20 mW and at 1064 nm above 20 mW.

The second configuration [33] does not use levitation, but instead the magnetic interaction force between a permanent magnet fixed above a PyC tile placed on the balance pan of scales. The optical power is proportional to the mass change which corresponds to a magnetic repulsion force change acting on the PyC tile irradiated by a laser beam. The photo-response sensitivity of this laser power sensor is about 100 mW mg⁻¹ and its discrimination threshold is about 1 mW. The main quantities influencing the measurement are wavelength, spot position on the PyC surface and power density of the laser under test. The relative uncertainty of the optical power measurement at 1064 nm decreases from 2% at 0.1 W to 0.8% at 1 W. This measurement uncertainty is quite like that of photodiode and thermopile sensors. However, the setup using accurate scales is not simple to use. Figure 7a shows a photograph of the set-up for the second experimental configuration. An example of response in terms of mass after 60 s irradiation for three different laser powers at 1064 nm is given in Figure 7b.

6.2 Diamagnetic spring

The third configuration [34] when its physical parameters (moment of inertia, natural frequency, logarithmic decrement, etc.) are determined could provide an absolute power measurement without calibration unlike to the two configurations presented in Section 6.1 which need to be calibrated by using laser sources and optical power meters as a reference. It uses the diamagnetic spring composed of a PyC piece levitated above a permanent magnet array. In this case, the PyC piece itself must not be irradiated by the laser beam under test. Figure 8a shows a photograph of an experimental setup of this inexpensive, sensitive, passive laser power meter. The measurement of radiation force is based on a torsional spring-mass-damper system consisting of a PyC disc (Ø = 20 mm) levitated above a NdFeB magnet array.

The nine-magnet array provides a magnetic field distribution with a 2D periodicity of the vertical component of the magnetic flux \( B_z \). The levitation force of the PyC disc is due to the interaction of the PyC diamagnetism in \( B_z \) and its 2D periodicity allows stabilizing the PyC disc over the center of the magnet array. To provide a steady angular position and thus a torsional restoring force, three holes (Ø = 1.5 mm) were drilled at the vertices of an equilateral triangle in the PyC disc. These holes are used to locate three polyamide spheres.

The measurement method is dynamic consisting in analyzing the response of the system to a rising or a failing
edge of a periodically interrupted laser beam. In this way, the angular response of the PyC disc to laser power remains linear over the measurement range. Figure 8b shows an example of response.

The first experimental results give a relative expanded uncertainty for measurement of optical power of 10% at 450 mW and 5% at 1 W and suggest an accuracy of 1% could be achieved for 5 W. Amongst the main sources of uncertainty are the moment of inertia of the levitated system and the measurements of the PSD voltage and the pseudo-period of the damped oscillation.

However, several parts of this device could be improved to reduce the laser power measurement uncertainty. These include:

- the techniques used for dimensional measurements to calculate the optical lever arms (from mirror for detection to PSD sensor and from mirror for laser under test to the rotation centre of the levitated part) and the moment of inertia of the levitated elements (PyC disc, polyamide spheres, cover glass, right-angle prism mirror);

- the detection sensitivity by using a longer cover glass to increase the optical lever arm and by using a new PSD sensor (more linear and more sensitive);

- the response linearity not only by using the new PSD but also by placing the right-angle prism mirror used for deflecting the detection laser beam at the rotation centre (it is not the case in Fig. 8a).

In this way, a relative expanded uncertainty of 1% for a smaller optical power than 1 W should be achievable, making this device potentially a very competitive measurement standard.

The main constraint for these three configurations is that they can work only when the PyC piece is perfectly adjusted in the horizontal plane. Consequently, the direction of the laser beam under test must be adjusted too with respect to the PyC piece.

7 Discussion and conclusion

The anisotropic diamagnetism of PyC allows one to use stabilized levitation at ambient temperature with no need...
for superconductors and their associated energy input and thus at very low cost. This remarkable property can be used for linkage devices and sensing. Some examples of applications show it could be interesting for metrology to use the diamagnetism of PyC as the sensitive element of various gauges.

All these sensors are used for measuring mechanical quantities such as acceleration, force, inclination, density or viscosity. Most of them are composed of an inexpensive primary sensor using magnets and PyC tiles combined with a secondary sensor. The PyC-based sensor is directly sensitive to the physical quantity to be measured and in general its response to a stimulus is a displacement (translation or rotation). The secondary sensor is often an optical sensor with a transducer delivering an electrical signal used to measure either a linear displacement or an angular deflection.

As with most sensors, environmental conditions (temperature, vibration, draughts, etc.) can have a more or less great effect on magnetic levitation and thus on the measurement results obtained with magnetic levitation sensors. Their influence must be reduced to obtain the best measurement accuracy. It is usually necessary to add sensors to measure quantities affecting accuracy in order to apply corrections to the measurement signal. Feedback systems can be also used to improve the accuracy of the PyC-based sensors. This is the case for instance for the accelerometer presented above, but also for the laser power sensor using a balance which has an internal feedback system maintaining the balance pan at a constant height.

Our recent and ongoing work at the LCM-LNE/CNAM has demonstrated the feasibility of measuring laser powers using PyC diamagnetism. Two effects can be used for this:

- Photo-thermal excitation of electrons induced by direct irradiation of the levitated PyC sheet, in this case the magnetic interaction force change which can be measured in terms of either levitation height change or mass change is related to the optical power of the laser beam.

- A diamagnetic spring related to the stiffness of the levitation force, in this case the levitated PyC sheet is used as a rotational spring pendulum for which the angular deflection is proportional to radiation pressure provided by a laser beam.

To conclude, this paper has shown that the main advantage of the PyC diamagnetism is to provide a low-cost element sensitive to motion in terms of inertia or inclination and force due to restoring magnetic force. To exploit its sensitivity, it must be associated with a suitable displacement detection and possibly a feedback system too.

Most of examples of PyC-based sensors presented in this paper remain laboratory sensors, not yet implemented in a routine way in metrology. Of course, while PyC diamagnetism is used in many applications to stabilize position, steer movement or avoid friction, it is rarely used as the sensitive element for measuring a physical quantity.

There might be other potential applications using PyC levitation for measurement and control for a wide range of instruments such as flowmeters, gravity meters, magnetometers or micrometers. In addition, as suggested by Küstler [35], recent developments in the new technology of printing magnet field domains could offer new opportunities of applications for metrology.

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