Ultrafast imaging of terahertz electric waveforms using quantum dots

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Abstract

Microscopic electric fields govern the majority of elementary excitations in condensed matter and drive electronics at frequencies approaching the Terahertz (THz) regime. However, only few imaging schemes are able to resolve sub-wavelength fields in the THz range, such as scanning-probe techniques, electro-optic sampling, and ultrafast electron microscopy. Still, intrinsic constraints on sample geometry, acquisition speed and field strength limit their applicability. Here, we harness the quantum-confined Stark-effect to encode ultrafast electric near-fields into colloidal quantum dot luminescence. Our approach, termed Quantum-probe Field Microscopy (QFIM), combines far-field imaging of visible photons with phase-resolved sampling of electric waveforms. By capturing ultrafast movies, we spatio-temporally resolve a Terahertz resonance inside a bowtie antenna and unveil the propagation of a Terahertz waveguide excitation deeply in the sub-wavelength regime. The demonstrated QFIM approach is compatible with strong-field excitation and sub-micrometer resolution—introducing a direct route towards ultrafast field imaging of complex nanodevices in-operando.

Introduction

The detection of radiation—including human vision—is typically sensitive to the energy carried by an electromagnetic wave rather than its fields. Heinrich Hertz succeeded to prove the existence of electromagnetic fields by conversion into incoherent visible fluorescence1. Today, electric waveforms can coherently be sampled with ultrashort laser pulses2–4 to directly access the temporal signatures of charge motion and quasi-particle excitations in condensed matter systems up to the visible spectrum5. Yet, relevant field distributions are often confined to microscopic scales significantly below the diffraction limit—arising from inhomogeneity of materials, microstructures or intrinsic confinement of light-matter excitations6–8. Only a few approaches spatially resolve local electric near-field waveforms up to multi-Terahertz frequencies, including raster-scanned photoconductive switches and electro-optic microscopy9–13. Enhanced resolution is provided by scattering near-field optical microscopy14–17, THz-driven scanning tunneling microscopy18,19 and recently emerging ultrafast electron microscopy20–22. THz-induced visible luminescence has been employed for imaging spatial field distributions via temporally cumulated effects of strong local fields23–26. Sampling THz electric waveforms in the time-domain using visible fluorescence appears highly desirable as it bears numerous prospects including the access to nanoscopic scales, 3D geometries, high-speed acquisition, and compatibility with strong local fields inside active and nonlinear-driven devices27–30.

Here, we demonstrate ultrafast far-field imaging of THz electric near-fields using fluorescence microscopy. We capture visible photons from local quantum dot probes and acquire stroboscopic movies of electric near-field evolutions. The scheme employs the quantum-confined Stark effect (QCSE)31–33, encoding electric near-fields...
Our experiments are based on two-color excitation using single-cycle Terahertz pulses to drive phase-stable near-fields and visible fs-pulses to excite the quantum dot probes, see Fig. 1a. The incident THz pulses at electric field strengths up to 400 kV/cm are enhanced in lithographically patterned gold structures. Colloidal CdSe-CdS core-shell nanocrystals, similarly used in voltage sensing applications\textsuperscript{26,34,35}, are deposited as a homogeneous layer of quantum-probes via drop-casting. Luminescence is excited via wide-field illumination in the image plane of a fluorescence microscope with \nobreak~150 fs pulses at wavelengths around 500 nm. We acquire differential images of the emission yield with a CCD camera in the presence and absence of THz excitation. The difference signal, which we refer to as the QFIM signal $S_{\text{QFIM}}$ in the following, represents the crucial observable for instant local fields.

First, we follow the ultrafast near-field evolution inside a THz antenna structure, shown in Fig. 2a, with sub-cycle temporal resolution by acquiring a sequence of snapshot images at increasing delays between THz and visible pulses. Figure 2b shows nine exemplary frames out of a series with temporal separation of $\Delta t = 30$ fs (full movie in Media 1). We observe a strong enhancement in the antenna gap and close to the terminal bars (THz polarization $\sim 0^\circ$ to the antenna axis). The signal is maximized at the edge of each antenna leg and decays symmetrically towards the center of the bowtie as apparent in the snapshot at $\Delta t = 0$ fs in Fig. 2c, demonstrating a spatial resolution of \nobreak~2 $\mu$m (see Supplementary Information). This pattern visually matches finite-element simulations of the THz electric near-field, shown in Fig. 2d, and strongly depends on the incident polarization (data for THz polarization $\sim 90^\circ$ to the antenna axis in Supplementary Information). Based on the simulated field enhancement and the incident peak field of \nobreak~400 kV/cm, we estimate a maximum near-field strength of \nobreak~10 MV/cm.

Analyzing the QFIM signal inside the gap, we demonstrate the extraction of local electric waveforms and characterize the temporal response of the bowtie antenna. As a prerequisite, we study the relation between the maximum field strength $F$ and the peak signal of $S_{\text{QFIM}}$. Measurements with varying incident field strengths yield the dependence $S_{\text{QFIM}} \propto F^{1.9}$ for the quantum dots used in the experiment, as evident in the double-logarithmic representation in Fig. 3b. Thus, the peak signal scales nonlinearly with the maximum incoming field\textsuperscript{34}. Employing the rectifying relation and the incident far-field waveform—obtained from calibrated conventional electro-optic sampling (EOS)—, we simulate the local near-field and the resulting QFIM signal using a finite-element time-domain simulation of the structure and find close agreement with the experimental QFIM trace, see Fig. 3a. The comparison of the incident THz waveform...
quasi-instantaneous interactions were previously repre-
strained by sub-wavelength geometries. In the infrared spectrum, these highly localized excitations arise from the propagating THz gap excitation inside a micro-slit. The localized THz resonance of a bowtie antenna and (b) the mechanism, we perform spatially resolved time-
temporal resolution by acquiring a sequence of snapshot images resolve the spatio-temporally evolution of the near-field.

The THz-induced change in the QD band structure can increase the absorption and translates to enhanced luminescence. Analyzing the QFIM signal inside the gap, we demonstrate the extraction of local electric waveforms and field strengths yield E_max near ~10 MV/cm.

Now, we demonstrate the field-resolved tracking of propagating ultrafast THz excitations using the QFIM scheme. Specifically, we spatio-temporally resolve a THz wavepacket traveling along the subwavelength slit of a gold waveguide, as depicted in Fig. 4a. We map the temporal evolution of the QFIM signal along the gap in a 2D representation (x, Δτ) in Fig. 4b, resolving two distinct features: First, the horizontal lines arise from the direct field enhancement inside the gap extending over the THz lengths around 500 nm. We acquire differential images of the emission yield with a CCD camera in the presence and absence of THz excitation. The difference signal, which we refer to as the QFIM signal (ΔS), can be detected via wide-field electro-optic sampling (EOS) and the peak signal of the THz electric near-field waveform (green) and the simulated local near-field (red) is shown in Fig. 2d. The simulated near-field distribution at resonance in the gap region closely resembles the QFIM signal in (c). A snapshot acquired in transient transmission contrast (Δτ = 0 fs) corroborates the field-driven absorption modulation as the origin of the QFIM signal.

We characterized the temporal response of the bowtie antenna. a Local QFIM signal in the gap of the bowtie (blue circles) and the modeled temporal luminescence evolution (gray) based on the incident waveform. b Scaling of the peak QFIM signal (circles) as a function of the maximum incident field strength. c Comparison of the driving far-field waveform (green) and the simulated local near-field inside the bowtie gap (red). d Corresponding spectra of both waveforms shown in (c) and the simulated near-field evolution is shown in Fig. 3c with corresponding spectra in Fig. 3d. Alternatively, a reconstruction of the near-field in a resonator can be obtained by adapting a single resonance model to the QFIM data, as shown in the Supplementary Information. Depending on the signal quality, direct extraction of near-field waveforms appears feasible via recovery of the polarity and reversal of the nonlinear QFIM signal.

The underlying mechanism enabling the QFIM scheme relies on THz-driven modulations of the electronic band structure in low-dimensional quantum systems, i.e., the QCSE in semiconductor nanocrystals. The altered electron and hole wavefunctions induce a quasi-instantaneous change of the optical transition dipole moment. As a result, the photoabsorption may be reduced or enhanced depending on the visible excitation frequency and the accessed electronic states, as previously resolved via transient absorption spectroscopy. We spatially map these changes via luminescence emission microscopy. Specifically, we note that irrespective of much longer luminescence lifetimes (~10 ns), the temporal sampling resolution is exclusively governed by the ultrafast absorption process. This quasi-instantaneous absorption can alternatively be accessed via transient absorption imaging of the antenna, as shown, e.g., for Δτ = 0 fs in Fig. 2e, yielding a pattern complementary to the QFIM signal.
focus. Subsequently, the tilted feature reveals the propagation of a THz gap excitation with a velocity $c_{\text{prop}}$ below $c_0$ emerging from the left edge of the structure. Such propagating plasmonic excitations are confined inside a subwavelength slit and provide the basis for ultrafast circuits—enabling the routing, nanofocusing, and enhancement of infrared radiation\(^{12,38–42}\). We corroborate our finding with a time-domain electromagnetic simulation of the ultrafast interaction (see “Materials and methods”), yielding the launching of a THz wavepacket from the edge with a propagation velocity $c_{\text{prop}}$ (white solid line in Fig. 4b) in agreement with the experimental QFIM dataset. This gap excitation manifests as a spatially oscillating electric field distribution along the slit—in contrast to the unidirectional field of the direct enhancement, illustrated by the simulated fields at two exemplary temporal delays ($\Delta \tau_1 = 0$ ps, $\Delta \tau_2 = 1$ ps) in Fig. 4d. In correspondence to Fig. 4b, c, we present the simulated electric near-fields as a spatio-temporal map in Fig. 4e. The simulation yields a phase velocity of the waveguide excitation between the vacuum and the substrate of $c_{\text{prop}} \sim c_0/2$. Moreover, we also reproduce the experimentally observed interference of the direct and the propagating pulses. We attribute the different propagation lengths of experiment and simulation to the idealized homogeneous microstructure assumed in the model\(^{43}\). Furthermore, the simulation yields a second gap excitation at the opposite side of the THz waveguide. We experimentally resolve this feature in a QFIM measurement acquired at the right side of the waveguide in Fig. 4c.

**Discussion**

We introduce Quantum-probe Field Microscopy to image ultrafast electric near-field waveforms in the time-domain. Our approach utilizes the encoding of momentary THz-fields onto the visible emission of nanocrystals and far-field fluorescence imaging. The underlying THz field-driven and quasi-instantaneous QCSE provides a direct link between the luminescence observable and the local electric fields. On this basis, we demonstrate the time-resolved microscopy of near-field waveforms inside a single bowtie antenna—a building block of ultrahigh-frequency devices, metamaterials, and strong-field light-matter interaction experiments\(^{27,28}\). Moreover, we observe
THz propagation inside a gap deeply in the subwavelength regime and, thus, introduce the ultrafast sampling of propagating electric fields inside confined structures in the time domain. These results motivate the application of QFIM for imaging electric waveforms of surface excitations, including THz phonon and plasmon polaritons on bulk surfaces and 2D heterostructures\(^4\).\(^5\). In contrast to near-field scattering microscopy based on nanotips, our scheme is compatible with strong driving fields and we envision unprecedented insights to THz-driven nonlinear dynamics, such as interactions between polaritonic wavepackets\(^7\),\(^29\). Finally, we highlight the prospect of QFIM for imaging THz fields at the nanoscale using optical super-resolution microscopy\(^46\), paving a promising way towards ultrafast nanoscopy of strong electric fields inside nonlinearly driven nanosystems.

**Materials and methods**

**Ultrafast QFIM microscope**

We generate high-field single-cycle THz pulses by the tilted pulse front method\(^47\) in a MgO:LiNbO\(_3\) crystal using pulses from an amplified 10 kHz Yb-laser system (central wavelength 1030 nm, pulse energy 1 mJ), see Fig. S1 in the Supplementary Information. For the quantum dot excitation, we employ laser pulses from an optical parametric amplifier (OPA) at 530 nm or 480 nm wavelength, optimized for QFIM signal strength. The vertically polarized THz beam is focused on the sample with a 90°-off-axis parabolic gold mirror. We obtain a maximum field strength of 400 kV/cm in the sample plane and a peak frequency of ~0.9 THz via calibrated EO sampling using a 100 µm thick <110> GaP crystal. In addition, the THz field strength can be varied by polarization rotation of the pump pulses used for THz generation. The OPA beam provides wide-field excitation in the sample plane. Luminescence is collected by a microscope objective. We acquire luminescence images with a cooled CCD camera. The pump pulses used for THz generation are chopped at a few Hz, and we capture synchronized luminescence images with and without THz pumping. The consecutive image sequences are digitally subtracted to obtain the THz-induced difference signal. Ultrafast temporal resolution in this pump-probe scheme is obtained via scanning the temporal delay \(\Delta t\) between THz pump pulses and visible excitation pulses via a mechanical delay stage.

**Electromagnetic simulations**

We employ a finite element solver (COMSOL Multiphysics) to calculate the electric near-fields of the structures. The model for the bowtie resonator consists of the gold antenna on a soda lime glass substrate\(^48\),\(^49\). For the propagating THz waveguide excitation, we employ a model consisting of two conducting metal bars (periodicity 50 µm, length 700 µm, gap 2 µm) on a soda lime glass substrate. We excite the structures using a plane wave single-cycle THz pulse (polarization perpendicular to the gap, center frequency 0.9 THz).

Details on the fabrication of gold microstructures, the synthesis of CdSe-CdS quantum dots and the polarization dependence of the bowtie antenna are presented in the Supplementary Information.

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**Author contributions**

M.B.H. and G.H. conceived the experiment. N.K. synthesized and characterized the quantum dots. T.L. fabricated the microstructures. J.A.L. and M.B.H. performed numerical near-field simulations. M.B.H. recorded the QFIM data. M.B.H. and G.H. analyzed the data and drafted the manuscript. All authors contributed to the interpretation of the data and the writing of the final manuscript.

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**Conflict of interest**

The authors declare no competing interests.

**Supplementary information**

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