Measuring bulk and surface acoustic modes in diamond by angle-resolved Brillouin spectroscopy

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The acoustic modes of diamond are not only of profound significance for studying its thermal conductivity, mechanical properties, and optical properties, but also play a definite role in the performance of high-frequency and high-power acoustic wave devices. Here, we report on the bulk acoustic waves (BAWs) and surface acoustic waves (SAWs) of single-crystal diamond using angle-resolved Brillouin light scattering (BLS) spectroscopy. We identify two high-speed surface skimming bulk waves (SSBW) with acoustic velocities of 1.277×10^6 and 1.727×10^6 cm/s, respectively. Furthermore, we obtain the relationship between the velocity of arbitrary BAWs and that of BAWs propagating along the high-symmetric axis at different incident angles. In the community of diamond-based acoustic studies, our results may provide a valuable reference for fundamental research and device engineering.

diamond, acoustic waves, angle-resolved Brillouin spectroscopy

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1 Introduction

Bulk acoustic waves (BAWs) and surface acoustic waves (SAWs) are caused by density fluctuations in the matter and provide information about the elasticity, electrostriction, and thermal capacity of materials [1-3]. In communication and sensing devices, both BAW-based and BAW-based devices, such as acoustic radio frequency (RF) filters, resonators, and SAW microelectromechanical systems (MEMS), have been extensively applied [4-9]. The use of micro-acoustic devices considerably reduced the size of signal processors in the communications field. With the rapid development of mobile communications, additional high-frequency and high-power acoustic wave devices will be required [10].

Diamond shows excellent performance in high-frequency and high-power acoustic wave devices because of its superhigh elastic modulus and thermal conductivity, stable chemistry, and low thermal expansion coefficient and dielectric constant [11]. In high-frequency and high-power SAW devices, piezoelectric film/diamond multilayer structures have been extensively applied [12-14]. Furthermore, the emergent study of quantum acoustodynamics (QAD) cavities based on diamond contributes to the development of hybrid quantum devices [15,16]. The spins of single nega-
tively charged Si vacancy (SiV) center [17,18] and nitrogen vacancy (NV) center [19,20] have a long coherence time, and these defects have achieved coherent interaction with SAWs. Therefore, additional research on the acoustic and physical properties of diamond is of great significance for designing high-performance acoustic wave devices.

Inelastic light scattering [21] is a precise method to detect phonons in solid materials. High-resolution Brillouin light scattering (BLS) spectroscopy is a noncontact, powerful method that has been extensively used to detect acoustic waves at frequencies of <300 GHz [3]. Two mechanisms contribute to the BLS process: scattering from BAWs through the elasto-optic mechanism, scattering from SAWs and SSBWs via the surface ripple [22]. In the past few decades, multiple different techniques, such as inelastic neutron scattering [23], inelastic synchrotron scattering [24], and ultrasonic pulse [25], have been used to investigate BAWs of solids. Compared with these techniques, BLS is more accurate and can measure acoustic signals at lower frequencies. Therefore, researchers prefer to use BLS to measure the acoustic properties of matter.

Prior research has used BLS to examine the BAWs of diamond. Grimsditch and Ramdas [26] measured BAWs along the high-symmetry direction of diamond and examined its elastic moduli and elasto-optic constants, but did not provide information of BAWs in other directions. Motochi et al. [27] obtained two SAW-like modes of chemical vapor deposition (CVD) diamond in BLS experiments; however, they did not explain the origins of these SAW-like modes. Therefore, it is necessary to explore angle-dependent properties of BAWs and investigate the physical mechanism of SAWs of diamond. Such a study should benefit the development of acoustic devices based on diamonds.

In this study, we report the angle-resolved BLS spectra of BAWs and SAWs of a diamond single-crystalline sample ((100) oriented) placed on a pristine Si wafer ((111) oriented). This study aims to explore the BAW frequencies of diamond dependent on the angle of incident light and explain the origins of two high-speed acoustic modes. With an increase in incident angle, the longitudinal acoustic (LA) peak shows a blueshift trend while the transverse acoustic (TA) peak gradually splits into two branches. We attribute this phenomenon to the velocity diversity of the acoustic mode along different crystal directions. Furthermore, we identify three modes propagating along the surface: Rayleigh SAW (RSAW), surface skimming transverse wave (SSTW), and surface skimming longitudinal wave (SSLW) whose velocities are 1.080×10^6, 1.277×10^6, and 1.727×10^6 cm/s, respectively.

2 Experimental details

Figure 1 shows our experimental setup, and we use a confocal microscope system to measure the BLS spectra of diamond in the backscattering geometry. The system is composed of high contrast (-10^{-15}) (3+3)-pass tandem Fabry-Pérot interferometers (FPI) and a confocal microscope (CM) with a 20× bright field objective lens (numerical aperture N.A=0.42) both from JRS Scientific Instruments in Switzerland. The detector is a Hamamatsu H10682-110 with a quantum efficiency of 10.8%. When the laser passes through the polarizing beam splitter (PBS), the s-polarized light is almost totally reflected to reach the sample while the p-polarized component is nearly completely transmitted. The incident light is emitted from a single longitudinal mode laser source at 532 nm and focused on the top surface of the diamond. The confocal setup assures that the collected scattering information is from as near to the surface as possible. Although the laser power is 29 mW, we did not observe any laser heating effect on the sample owing to the high thermal conductivity of diamond. In our experiments, there are three polarization configurations: circular polarization (σ+σ−), parallel polarization (VV), and cross polarization (VH). The three polarizations correspond to only the quarter wave plate (QWP) in the light path, both the QWP and polarizer in the light path, as well as neither the QWP nor polarizer in the light path. Here, the first and second items of polarization abbreviation describe the polarization of the incident and scattered light, respectively. In particular, σ+ (σ−), V, and H represent right (left) circular polarization, s-polarization, and p-polarization, respectively.

A 3 mm×3 mm×0.25 mm diamond, purchased from Element Six Technologies of the Anglo American PLC, is a type IIa single crystal synthesized by CVD. It has extremely low dislocation density and defect concentration, where the boron concentration is <0.05 ppm and the nitrogen concentration is <0.01 ppm.

**Figure 1** (Color online) Experimental setup. Only the s-polarized component of incident light is completely reflected by the PBS and finally focuses on the diamond surface. The inset is a schematic diagram of light and phonon wave vectors on the x-y plane, where phonons include SAW (wave vector is qS) and BAW (wave vector is q). θi is the refraction angle inside the diamond.
centration is <1 ppm. There are two (100) oriented surfaces that are polished with a roughness <30 nm and the 12 edges are along the <100> orientation with miscuts within 3°. The diamond is placed on a Si wafer and then fixed on a home-built angle-resolved holder that can be rotated around the z-axis, as shown in Figure 1. The incident angle θ \_i is adjusted by rotating the diamond to achieve angle-resolved BLS measurements. The rotation accuracy is <1°. The parameters of the diamond are density ρ=3.515 g/cm³ and refractive index n=2.426 when λ=532 nm.

### 3 Results and discussion

BLS is an inelastic scattering of light from acoustic phonons because of the density fluctuations of materials [28,29]. In the Brillouin shift, the frequency f of a scattered acoustic wave is written as follows:

\[ f = qv, \]

where \( v = \sqrt{X/\rho} \) is the acoustic velocity; \( X \) is an expression composed of the elastic modulus \( C_{ij} \); \( \rho \) is the density of sample; and \( q \) is the magnitude of wave vector \( \mathbf{q} \).

For a given wave vector of incident light \( \mathbf{k} \), under back-scattering geometry, the detected BAW wave vector is \( \mathbf{q} = \pm 2\pi n \mathbf{k} \) and the SAW wave vector is \( \mathbf{q}^i = \pm 2\pi n \sin \theta_i \mathbf{k} \), where \( \theta_i \) is the incident angle [30]. Therefore, both \( \mathbf{q} \) and \( \mathbf{q}^i \) are equal to \( \pm 5.73 \times 10^5 \text{ cm}^{-1} \) and \( \pm 2.36 \sin \theta_i \times 10^5 \text{ cm}^{-1} \) in our BLS experiments, respectively, i.e., the BAW wave vector in the sample is a constant, while the SAW wave vector is proportional to \( \sin \theta_i \). Because of the nonnegligible numerical aperture of the objective lens, \( \mathbf{q}^i \) has an angle-dependent uncertainty \( \Delta \theta^i \). Under the given conditions, the magnitude of \( \Delta \theta^i \) is \( \Delta \theta^i = 2k \cos \theta_i \times NA \), where \( NA \) is the numerical aperture of the objective lens. Therefore, the spectra of SAW broadened at a smaller \( \theta_i \). The \( NA \) of our objective lens is 0.42, such that the SAW \( \Delta \theta^i \) is \( \sim 1 \times 10^5 \text{ cm}^{-1} \) under normal incidence. With \( \theta_i \) approaching 90°, the full width at half maximum (FWHM) of SAW decreases. Selecting an appropriate objective lens can effectively suppress such a broadening effect.

For an arbitrary propagation direction, there are two quasi-TA modes and one quasi-LA mode. Usually, LA mode propagates faster than the TA mode [3]. We list the acoustic velocities of diamond previously reported [24,25] and our measured velocities in Table 1. In the BLS spectra, the intensity and polarization properties of scattering signals are determined by the scattering tensors of the acoustic modes. Scattering tensors are dependent on the direction of wave vector \( \mathbf{q} \) of the scattered acoustic phonons. For \( \mathbf{q} \) parallel to the [100] orientation, the scattering tensors \( T \) of BAWs along three different vibration directions are listed below:

\[
\begin{align*}
LA: \quad \mathbf{u} &= [100], \quad T = q^2 \begin{bmatrix} 0 & 0 & 0 \\ 0 & p_{12} & 0 \\ 0 & 0 & p_{12} \end{bmatrix}, \\
TA_+: \quad \mathbf{u} &= [001], \quad T = q^2 \begin{bmatrix} 0 & 0 & p_{44} \\ 0 & 0 & 0 \\ p_{44} & 0 & 0 \end{bmatrix}, \\
TA_-: \quad \mathbf{u} &= [010], \quad T = q^2 \begin{bmatrix} 0 & p_{44} & 0 \\ p_{44} & 0 & 0 \\ 0 & 0 & 0 \end{bmatrix},
\end{align*}
\]

where \( \mathbf{u} \) is the vibration direction of phonons traveling along \( q \), \( \varepsilon_0 \) is the dielectric constant of the material, and \( p_{ij} \) is the elasto-optic constant. Under a given polarization configuration, the intensity \( I \) of a scattered peak is proportional to \( [\varepsilon_s \cdot T \cdot \varepsilon_i]^2 \), where \( \varepsilon_s \) and \( \varepsilon_i \) are unit vectors along the polarization direction of the scattered and incident light, respectively. Under VV polarization, the \( [\varepsilon_s \cdot T \cdot \varepsilon_i]^2 \) of the LA mode is proportional to \( p_{44}^2 \) while both TA modes are undetectable; under VH polarization, only the \( [\varepsilon_s \cdot T \cdot \varepsilon_i]^2 \) of

| Propagation direction of \( q \) | Velocity of acoustic mode | Previous reports (×10^6 cm/s) | This work (×10^6 cm/s) | Vibration direction of mode |
|---|---|---|---|---|
| 100 (Γ-X) | \( v_{LA} \) | 1.751^{b}\ | 1.744±0.0005 | 010/001 |
| 110 (Γ-K) | \( v_{TA} \) | 1.282^{b}\ | 1.268±0.0001 | 100 |
| 110 (Γ-L) | \( v_{TA} \) | 1.833^{b}\ | 1.822±0.0042 | 110 |
| 111 (Γ-A) | \( v_{LA} \) | 1.282^{b}\ | 1.268±0.0003 | 001 |
| 100 → 110 (Γ-A) | \( v_{LA} \) | 1.857^{b}\ | – | 111 |
| 100 → 110 (Γ-A) | \( v_{LA} \) | 1.208^{b}\ | – | 110/112 |
| 100 → 110 (Γ-A) | \( v_{LA} \) | – | 1.744-1.784 | – |

a) Calculated by \( v_{LA} = \sqrt{C_{44}/\rho} \) and \( v_{TA} = \sqrt{C_{44}/\rho} \) where \( \rho=3.512 \text{ g/cm}^3 \) is the density of diamond in this study. The elastic moduli \( C_{44} \) and \( C_{11} \) are cited from ref. [25].

b) Ref. [24].

Table 1 Acoustic velocity of diamond
the TA₁ mode is not zero; and for σ⁺σ⁻ polarization, all modes can be measured.

Figure 2(a)-(c) show the angle-resolved BLS spectra of diamond under three polarization configurations. The LA mode is undetectable in VH polarization and the TA mode is not detected in VV polarization. When the laser is perpendicularly incident on the sample surface (i.e., θᵢ=0), the measured frequencies of LA and TA modes are ~159 and ~116 GHz, respectively. Based on the measured frequency, we report that their velocities are consistent with LA and TA modes along the Γ-X direction [25]. With increasing θᵢ, the frequency of the LA mode has a blueshift, and the TA mode gradually splits into two peaks: one with an unchanged frequency at 116 GHz and the other with a redshift, as shown in Figure 2(d)-(g). Gradually, the A, B, and C modes appear on the spectra with increasing θᵢ and their frequencies are possibly proportional to θᵢ, as shown in Figure 2(h). In Figure 2(i), A and B modes are close together and almost merge into one broad peak, which has a VH polarization. Here, we only show the spectra of A and B modes under VH polarization because spurious signals affect the analysis of peaks in the 30-40 GHz range for both VV and σ⁺σ⁻ configurations.

Figure 3(a) shows the 1/8 zone of the first Brillouin zone (BZ) of the diamond [31]. Because the point group of the diamond belongs to O₈ with 48 symmetry elements: the first BZ can be divided into 48 equivalent irreducible wedges (IW) [32]. The IWs are shown as the shaded area in Figure 3(a) and bounded by the three high symmetry axes, Γ-X, Γ-K, and Γ-L. Each IW contains all BAWs in the diamond. As per our experimental geometry, the wave vectors of incident light and scattering light vary in the x-o-y plane of the IW. As shown in Figure 3(b), the measured BAWs propagate along or against the direction of refracted light (Γ-A direction) with a velocity of vₐx. Therefore, the wave vector of scattered
phonons $q_{\text{FA}}$ is a linear combination of $q_{\text{FX}}$ and $q_{\text{FK}}$, and $v_{\text{FA}}$ is the vector sum of $v_{\text{FX}}$ and $v_{\text{FK}}$. Table 1 lists the velocities of the TA and LA modes along the Γ-A direction. In a parallelogram ACTD with a 45° angle, we can easily find that:

$$v_{\text{TA}} = v_{\text{FX}} \cos \theta_i + v_{\text{FK}} \cos (45° - \theta_i),$$  \quad (5)$$

where $q_{\text{FX}}$ and $q_{\text{FK}}$ are two components of $q$ propagating along the Γ-X and Γ-K directions, while $v_{\text{FX}}$ and $v_{\text{FK}}$ are the velocities along the Γ-X and Γ-K axes, respectively. It is more important to obtain the velocities using the incident angle rather than the refractive angle:

$$v_{\text{TA}} = v_{\text{FX}} \left( n_i^\text{X} - n_i^\text{F} \sin \theta_i \right) \left( n_i^\text{X} - n_i^\text{F} \sin \theta_i \right)^{-1} + v_{\text{FK}} \left( n_i^\text{K} - n_i^\text{F} \sin \theta_i \right) \left( n_i^\text{K} - n_i^\text{F} \sin \theta_i \right)^{-1}.$$

(6)

where $n_0=1$ is the refractive index of air, $\theta_i$ is the incident angle between 0° and 90°, and the direction of diamond rotation around the z-axis cannot affect the sign of $v_{\text{TA}}$. When $\theta_i=90°$, $\theta'$ has a maximum $\theta'=24.3°$ based on Snell’s law. Thus, we cannot measure the real LA and TA modes traveling along the Γ-K direction. By establishing the connection between the high-symmetry axes in the BZ and an arbitrary direction in the crystal, eq. (6) provides a convenient method to calculate the velocity of BAWs propagating along an arbitrary direction. Note that the existence of Γ-W phonons cannot be totally excluded if their velocity has significant differences from $v_{\text{FK}}$. This effect will lead $v_{\text{FK}}$ in eq. (6) to change with $\theta_i$ and we can approximately write $v_{\text{FK}}$ as $v_{\text{FK}}=v_{0}+\alpha \sin \theta_i$. Here, $v_0$ is the value of $v_{\text{FK}}$ determined at $\theta_i=0$ and $\alpha$ is the $\theta_i$-dependent coefficient of $v_{\text{FK}}$ when $\theta_i$ increases from 0° to 90° because of the contribution from the ΓW phonon. As $\theta_i$ increases, the value of $v_0+\alpha \sin \theta_i$ will be close to actual sound velocity along the ΓK direction.

In Figure 3(c), we fitted the velocity data of three BAWs with the revised eq. (6). Parameters are obtained by fitting: for the LA mode, $v_{\text{FX}}=1.744\times10^6$ cm/s and $v_{\text{FK}}=1.757+0.065 \sin \theta_i \times10^6$ cm/s; for the TA mode, $v_{\text{FX}}=v_{\text{FK}}=1.268\times10^6$ cm/s; for the TA mode, $v_{\text{FX}}=1.268\times10^6$ cm/s and $v_{\text{FK}}=1.173+3.46\times10^{-5} \cos \theta_i \times10^6$ cm/s. The $v_{\text{FK}}$ of the LA mode is more sensitive to the Γ-W phonon than that of the TA mode. When $\theta_i=90°$, $v_{\text{FX}}=1.822\times10^6$ cm/s and $v_{\text{FK}}=1.173\times10^6$ cm/s, almost coinciding with previous reports. When $f=5.73\times10^4$, we fitted frequency data of the three modes in Figure 3(d) and obtained the same conclusion, i.e., the velocity of the LA (TA) mode propagating along an arbitrary direction can be calculated with the vector sum method in IWs. In our experiments, the propagating direction of BAWs gradually changed from the Γ-X to Γ-K direction as $\theta_i$ increases. As shown in Table 1, for the LA mode, $v_{\text{FX}}<v_{\text{FK}}$; however, for the TA mode, $v_{\text{FK}}$ has two different values for two orthogonal vibration directions—one is equal to $v_{\text{FX}}$ and the other is smaller. Therefore, the LA peak is blueshift, the TA peak is split, and one of the TA peaks is redshifted during the rotation of the diamond sample.

In contrast to BAWs, SAWs are typical acoustic modes propagating along the surface. SAWs can be observed only when $k_i$ has a projection on the surface, i.e., $q_i$ is non-zero. Under the angle-resolved BLS configuration, $q_i$ gradually increases as the angle $\theta_i$ increases. We reported that A, B, and C modes have the characteristics of SAWs: their frequencies are almost 0 when $\theta_i=0$ and are obviously proportional to $\sin \theta_i$ as shown in Figure 4(b). Entropy fluctuation is a possible reason for the widening of Rayleigh lines at low angles [33]; however, it cannot explain the splitting of Rayleigh lines and the blueshift of these modes. As mentioned above, the SAW peaks are broadened because of the finite numerical aperture of the objective lens and the entrance aperture of the interferometer under a small $\theta_i$. We use the above dispersion relationship of SAWs to linearly fit the experimental data of these three modes and obtain their velocities: $v_{\text{A}}=(1.277\pm0.011)\times10^6$ cm/s, $v_{\text{B}}=(1.080\pm0.009)\times10^6$ cm/s, and $v_{\text{C}}=(1.727\pm0.010)\times10^6$ cm/s.

The B velocity mode meets the conditions of RSAW, which possesses a phase velocity of ~10% lower than that of the slower BAW (TA2 in this work) on the same substrate surface. RSAW is primarily caused by coupling of longitudinal (L-) and shear vertical (SV-) type BAWs close to the surface; therefore, most of the energy is concentrated close to the surface [7], as schematically shown in Figure 4(a). Jiang et al. [34] reported that the calculated velocity of RSAW is
The solid circles represent experimental data and the solid lines are fitting to the data. Djemia et al. [35] reported that RSAW is stimulated Brillouin scattering on polycrystalline CVD diamond film. The propagation direction of particles (VDP) is parallel to the surface. Notably, the velocity of SAW should be smaller than the slower TA mode [7], but the velocities of A and C modes are close to those of the TA and LA modes, respectively. Therefore, we can safely conclude that A and C modes are pseudo-BAWs [36] or surface skimming bulk waves (SSBWs) [7] in different applications. SSBWs originate from the components of BAWs propagating along the surface; however, their energy gradually leaks into the bulk at a propagation angle (the angle between the surface and the propagation direction) smaller than that of the leaky wave [37]. SSBWs are divided into surface skimming transverse waves (SSTWs) and surface skimming longitudinal waves (SSLWs) as per the different vibration directions. There are multiple SSBWs with different velocities in a plate-shaped material, and their velocities are related to the thickness of the plate and the thickness of the dielectric layer on the plate [36]. Here, our SSBWs could be from the interface between air and diamond layers. Because incident light is focused on the surface, the velocity of SSBWs should be between that of the TA mode and LA mode. The velocities of A and C modes in our work are almost the same as the velocities of the TA mode and LA mode of diamond, respectively. Moreover, as shown in Figure 2(a) and (b), the polarization property of A mode is similar to the TA mode. In this study, we examined acoustic velocities propagating along an arbitrary direction within a crystalline diamond with angle-resolved BLS spectroscopy. We determined the acoustic velocities of arbitrary BAWs as functions of the incident angle and the acoustic velocities of BAWs along the high-symmetry axis. As per the angle-resolved BLS spectra, we successfully identified three waves with SAW properties in the (100) face and discussed their physical mechanisms. Thus, the A mode is attributed to SSTWs, for which the vibration direction of particles (VDP) is parallel to the surface but perpendicular to the propagation direction of waves; the C mode is attributed to SSLWs [38], where the VDP is parallel to both the sample surface and the propagation direction of the wave, as shown in Figure 4(a). The propagation of SSBWs on substrates cannot be affected by surface roughness, and SSBWs have been applied to fabricate high-frequency and temperature-stable devices due to their high propagation velocity [39-41].

4 Conclusions

In this study, we examined acoustic velocities propagating along an arbitrary direction within a crystalline diamond with angle-resolved BLS spectroscopy. We determined the acoustic velocities of arbitrary BAWs as functions of the incident angle and the acoustic velocities of BAWs along the high-symmetry axis. As per the angle-resolved BLS spectra, we successfully identified three waves with SAW properties in the (100) face and discussed their physical mechanisms. Because SSBWs have a higher propagation velocity than RSAW, our results provide guidance for designing diamond-based surface acoustic devices with higher frequencies.
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