THE PAST AND FUTURE EVOLUTION OF A STAR LIKE BETELGEUSE

Georges Meynet, Lionel Haemmerlé, Sylvia Ekström, Cyril Georgy, José Groh and André Maeder

Abstract. We discuss the physics and the evolution of a typical massive star passing through an evolutionary stage similar to that of Betelgeuse. After a brief introduction recalling various observed parameters of Betelgeuse, we discuss the Pre-Main-Sequence phase (PMS), the Main-Sequence (MS) phase, the physics governing the duration of the first crossing of the HR diagram, the red supergiant stage (RSG), the post-red supergiant phases and the final fate of solar metallicity stars with masses between 9 and 25 \( M_\odot \). We examine the impact of different initial rotation and of various prescriptions for the mass loss rates during the red supergiant phase. We show that, whatever the initial rotation rate (chosen between 0 and 0.7 \( \times \nu_{\text{crit}} \), \( \nu_{\text{crit}} \) being the surface equatorial velocity producing a centrifugal acceleration balancing exactly the gravity) and the mass loss rates during the RSG stage (varied between a standard value and 25 times that value), a 15 \( M_\odot \) star always ends its lifetime as a RSG and explodes as a type II-P or II-L supernova.

1 Introduction

Betelgeuse (spectral type M2Iab) is one of the closest red supergiants and the subject of many studies. Its effective temperature is 3641±53 K obtained by infrared interferometry (Perrin et al. [2004]) and its luminosity is around Log \( L/L_\odot =5.10\pm0.22 \) deduced from its bolometric luminosity and its distance which is somewhat uncertain. The present luminosity value is deduced taking a distance of 200 pc (Harper et al. [2008]; see also the discussion in Le Bertre et al. [2012]). The ratios of the abundances of nitrogen to carbon is 2.9 (in mass fraction) and that of nitrogen to oxygen is 0.6 according to Lambert et al. [1984]. Typical solar values

1 Geneva Observatory, University of Geneva, CH-1290 Versoix Switzerland
2 ENS, Lyon, France

© EDP Sciences 2014
DOI: (will be inserted later)
are N/C=0.3 and N/O=0.1, thus clearly Betelgeuse shows signs of the presence of CNO processed material on its surface (nitrogen enhanced with respect to carbon and oxygen). The surface rotation velocity is about 5 km s\(^{-1}\) (Uitenbroek et al. 1998). According to Le Bertre et al. (2012), Betelgeuse has been losing mass at a rate of \(1.2 \times 10^{-6} \, M_\odot\) per year for the past 80,000 years. The surface magnetic field is \(\sim 1\) Gauss (Aurière et al. 2010). In the following we shall discuss what was the past evolution of such a star, as well as what will be its future evolution.

2 The Pre Main-Sequence phase with accretion

Stars are formed from the collapse and fragmentation of large molecular clouds. The collapse being non-homologous, hydrostatic equilibrium is first reached by a
Past and future evolution of Betelgeuse

central core. The core then grows in mass through accretion of part of the infalling material. Today, it is believed that this scenario is occurring for low, intermediate, and also for massive stars (e.g. Beech & Mitalas 1991, Bernasconi & Maeder 1996, Yorke & Bodenheimer 2008, Kuiper et al. 2010).

A possible pre-MS evolutionary track in the HR diagram for such a star can be seen in Fig. 1. The heavy line on the right of this plot is the birthline. It corresponds to the evolutionary track of an object increasing its mass through accretion. Here the accretion law is taken as in the work by Behrend & Maeder (2001). The computation started from a 0.7 M⊙ core. Typical accretion rates are between 10^{-5} and 10^{-3} M⊙ yr^{-1}. For assembling a 14 M⊙ star, it takes typically about 190 000 years. When, for whatever reason, accretion stops, the star becomes visible, hence the name of birthline given to the “accreting” evolutionary track. The object will then evolve to reach the Zero Age Main Sequence (ZAMS). This phase lasts about 100 000 years for the 14 M⊙ shown in Fig. 1. We see that for such a massive star, the “post birthline” phase, which is also the visible phase, is quite short. This comes from the fact that the accretion timescale is of the same order of magnitude as the Kelvin-Helmholtz timescale which gives the timescale for the contraction phase. For those stars, both processes, accretion and slow contraction towards the ZAMS, take more or less the same time and since they are occurring simultaneously when accretion stops the star is nearly already on the ZAMS. This becomes still more true for higher initial masses and above a mass limit which depends on the accretion rate we have that the accretion timescale becomes greater than the contraction time. In that case when contraction stops, part of the hydrogen in the core is transformed into helium (Bernasconi & Maeder 1996).

Haemmerlé et al. (submitted to A&A) has recently revisited the scenario of formation of stars through accretion by studying the effects of rotation during that phase. In addition of accreting matter, angular momentum is accreted. A very simple law of angular momentum accretion has been considered: the accreted material has the same angular velocity as the surface of the accreting object, no braking mechanism, like disk locking, is considered during the contraction phase. On the right panel of Fig. 1, we can see how the internal rotation evolves during the PMS phase. When the star reaches the ZAMS it has nearly a solid body rotation. We can compare the MS evolution obtained when the PMS phase with accretion is accounted for and when evolution begins on the ZAMS assuming that the star rotates as a solid body. Very similar results are obtained provided both models on the ZAMS have the same total angular momentum. So it means that, at least in the frame of the accretion scenarios explored by Haemmerlé et al., the hypothesis made in many computations, i.e. to start from a solid body rotating model on the ZAMS is quite justified.

3 The mixing during the Main-Sequence phase

In the recent years, many efforts have been made to study the impact of rotation on massive star evolution (see e.g. Langer 2012, Maeder & Meynet 2012, Chieff
Fig. 2. N/H ratio at the end of the MS as a function of the initial mass for all the models. Models at $Z = 0.014$ (left), $Z = 0.006$ (centre), and $Z = 0.002$ (right). Figure taken from Georgy et al. (in press for A&A). The different curves correspond to different initial velocities. From top to bottom, the angular velocity at the surface on the ZAMS corresponds to $0.95$, $0.9$, $0.8$, $0.7$, $0.6$, $0.5$, $0.3$, $0.1$ and $0$ times the critical angular velocity. The curves for 0 and 0.1 are superposed and cannot be distinguished. The curves labeled $\text{mid-H}$ correspond to the surface abundances when the mass fraction of hydrogen at the centre is 0.35, while the curves labeled $\text{end of H-b}$ correspond to the surface abundances when the mass fraction of hydrogen at the centre is 0.0.

& Limongi 2013 and references therein). One of the main effects of rotation is to allow some elements abundant in the core to reach the surface and inversely some others, abundant in the envelope, to be injected into the convective core. This has many consequences for the evolutionary tracks in the HR diagram, the lifetimes, the massive star populations, the nucleosynthesis, the properties of the final stellar collapse and of the stellar remnants. One way of checking the physics included in these models is to observe surface abundances and surface velocities of B-type stars and to see whether the observations agree with the predictions of the theoretical models (see e.g. Brott et al. 2011, Przybilla et al. 2010). For making easier the comparison, the observed sample must be composed of stars as similar as possible (i.e. same initial mass, initial composition, age, same magnetic field if any; no close companion) except for the velocity of rotation. When such precautions are taken, general good agreement is obtained between theory and observations (Maeder et al. 2009). Let us note that the check of the physics of rotation is very important not only to understand single star evolution but also close binary systems with rotating components.

We show in Fig. 2 how the nitrogen abundance varies at the surface of different
models. Without any rotation, all these models would present no enrichments, all the curves would be flat line in the grey zones. We note that rotational mixing increases with the initial mass, the initial rotation, with the age and when the metallicity decreases (see also e.g. Maeder & Meynet 2001). A star like Betelgeuse had very likely a rotating star as a progenitor, but was it a slow or a fast rotator? We shall discuss this point further below in this paper.

4 The first crossing of the HR diagram

The timescale which governs the crossing of the HR diagram after the MS phase depends on when He-ignition occurs. If the ignition only occurs when the star is in the red supergiant phase (when Log $T_{\text{eff}} < 3.7$), then the timescale for the crossing is given by the Kelvin-Helmholtz timescale and is quite short. On the contrary, when core He-ignition occurs when the star is still a blue supergiant, then the timescale is much longer because it is governed by the nuclear timescale. Now what are the main parameters which govern where in the HR diagram He-ignition occurs? There is a rich literature on the subject (Renzini et al. 1992, Stancliffe et al. 2009) and it is still a debated question. Here we discuss a few points without the ambition to be exhaustive.

In order for the envelope to expand and the star to evolve redwards in the HR diagram, some energy has to be injected in the envelope at a rate fast enough for preventing radiation to simply evacuate it (i.e. preventing that the energy simply flows in the envelope without heating some part of it). This “fast” energy injection mainly comes from the contraction of the core (part of it can come also from the H-burning shell but the rate of injection of energy is likely too slow and somewhat in continuity with the energy provided by the H-burning core). Among the factors that favors a weak expansion of the envelope and therefore a core He-burning phase occurring for a significant part in the blue part of the HR diagram, one notes:

- a low metallicity: if we consider the extreme case of Pop III stars, most of the core He-burning phase is spent in the blue part of the HR diagram (see e.g. Ekström et al. 2008). The reason is the following: in absence of CNO elements, H-burning occurs at very high temperatures, so high that some $3\alpha$ reaction takes place too. This produces some carbon and oxygen which then trigger the activity of the CNO cycle. It means also that the central temperature during the core H-burning phase is near the temperature for core He-burning. Thus, at the end of the MS phase, the core does not need to contract very strongly for igniting He. Thus small amount of energy is released by core contraction and the star remains in the blue part of the HR diagram during its core He-burning phase. Only at the very end of the core He-burning phase, contraction of the core makes the star to evolve into the red supergiant stage. Similar behavior, although less marked is expected for low (but non zero) metallicities.

- a small helium core mass: the smaller is the helium core mass with respect to
the envelope mass, the more difficult will be for the core to release sufficient energy by contraction to uplift its envelope.

- a weak opacity of the envelope: in case the envelope material is sufficiently transparent to radiation, then it would allow the excess energy released by the contraction of the core to be rapidly emitted away. This would prevent the inflation of the envelope.

- weak stellar winds: weak stellar winds allow the star to keep massive envelopes which are more difficult to inflate than less massive ones. Note however that very strong mass losses would uncover the H-rich envelope and conversely favor a blue location in the HR diagram.

- strong mixing: a strong mixing favors a blue location for the evolutionary tracks in the HR diagram. An illustration of this is the extreme case of homogeneous evolution which keeps the star in the blue part of the HR diagram (Maeder 1987). Fig. 4 shows the evolution of $T_{\text{eff}}$ as a function of age during the post MS-phase for 15 $\odot$ solar metallicity models. For $v_{\text{ini}}/v_{\text{crit}}=0$ and 0.4 , the models spend very short periods with $\log T_{\text{eff}} > 4.0$, while the model with $v_{\text{ini}}/v_{\text{crit}}=0.7$, in which the mixing is much stronger, spends about one third of the post-MS phase in the blue part of the HR diagram.

Depending on the way this first HR crossing occurs, stars enter into the RSG phase in a more or less advanced stage of their core He-burning phase. This has consequences for the lifetime of the RSG phase.

5 The red supergiant phase

When the star evolves into the red supergiant phase, as a result of the deepening of the outer convective zone and of mass loss, significant changes of the surface abundances are expected even in non-rotating models, as can be seen on the left panel of Fig. 3. In this panel, one can also see that red supergiants with masses below or equal to 15 $\odot$ present N/C and N/O ratios which are between initial values, 0.3 and 0.1 respectively, and maximum values equal to $\sim 3.1$ and 0.7 respectively. For masses equal and above 20 $\odot$, as a result mainly of strong mass loss during the red supergiant phase, much higher N/C and N/O ratios can be obtained.

Looking at the right panel, one sees that when rotation is accounted for (the typical time-averaged rotation velocities of the models during the MS phase are between 190 and 220 km s$^{-1}$), in the whole luminosity range considered, the N/C ratios (in mass fractions) are comprised between 2.2 and 9.5 and the N/O between 0.5 and 1.3. So rotation brings three main differences: first, the minimum values of the ratios are greater than the initial ones. This is of course due to the mixing occurring during the previous evolutionary phases. Second, the maximum values for stars with masses below 15 $\odot$ are slightly higher than those obtained in non-rotating models. Third, there are no longer red supergiants in the high luminosity
range presenting very high N/C and N/O ratios. This comes from the fact that the present rotating models for the 20 and 25 $M_\odot$ have very short RSG lifetimes, thus they do not have much time to lose important amounts of mass during that phase and thus to modify through mass loss their surface abundances during that phase.

Since observed populations are a mixture of stars with different initial velocities, one can expect some scatter of the N/C and N/O ratios observed for RSGs. Comparing the position of Betelgeuse with the evolutionary tracks shown in Fig. 3, we can note that rotation, through making the tracks more luminous for a given initial mass, tends to decrease the initial mass of Betelgeuse. Non-rotating model would associate a mass around 20 $M_\odot$, while the $\upsilon_{\text{ini}}/\upsilon_{\text{crit}}=0.4$ model would associate a mass around 15 $M_\odot$. Looking at Fig. 3, one sees also that the age associated to such a star would be between 11.5 and 12.5 My in case of non-rotating models, and between 15.1 and 15.7 My for $\upsilon_{\text{ini}}/\upsilon_{\text{crit}}=0.4$ models. The surface N/C and N/O ratios for Betelgeuse are framed by the values of the non-rotating 20 $M_\odot$ model (see points 20/1 and 2 on the left panel of Fig. 3) and are a little too low with respect to what is expected from rotating models (see points 15/1 and 15/2 on the right panel of Fig. 3), indicating that the progenitor of Betelgeuse could be a slower rotator than those shown on the right panel.

6 What does it happen after the red supergiant phase?

After the red supergiant phase, three different evolutionary scenarios may occur: 1) the star can stay in the red supergiant stage until it explodes as a type II-P supernova; 2) the star may make excursions in the blue part of the HR diagram through a blue loop evolving back to a red supergiant stage, exploding either as a type II-P or II-L supernova; 3) the star may end its stellar lifetime as a blue, yellow supergiant (Georgy 2012), LBV (Groh et al. 2013) or even a Wolf-Rayet star. Which one of these three scenarios is realized depend on mixing and mass loss. The effects of changes of mass loss rates during the RSG phase have been studied for instance by Vanbeveren et al. (1998), Salasnich et al. (1999), Yoon & Cantiello (2010). We show in Fig. 7 the tracks of 15 $M_\odot$ models at solar metallicity with different initial velocity and mass loss rates during the red supergiant stage. The standard model ($1 \times \dot{M}$) has been computed with the same mass loss prescriptions as in Ekström et al. (2012). The two other enhanced mass loss rate models have been computed multiplying by a factor 10 and 25 the mass loss rates as long as $\log T_{\text{eff}} < 3.7$.

Let us first comment the left panel presenting models without rotation. We see that enhanced mass loss during the RSG stage produces more extended blue loops in effective temperatures and also increase the duration of the blue loop phase. This is expected, since mass loss enlarge the fraction of the total mass of the star occupied by the core, and the mass fraction of the core is an important parameter governing the blue loop (Giannone 1967, Lauterborn et al. 1971): the larger this mass fraction is, the more important the loops are. The middle panel shows the situation when some moderate rotation is accounted for. We see first that the first
Fig. 3. **Left panel**: Evolutionary tracks for non-rotating solar-metallicity models during the red supergiant phases. For some points along the tracks, we have indicated the actual mass of the star, the mass fraction of helium at the centre, $Y_c$, the ratios of the abundances (in mass fraction) at the surface of nitrogen to carbon, $N/C$, and of nitrogen to oxygen, $N/O$. The pentagon shows the position of Betelgeuse using the data reported in the introduction. **Right panel**: Same as the left diagram for rotating models.

The crossing of the HR diagram is shorter than in the non-rotating case. This comes from the fact that for this moderate rotation rate, the cores are slightly enlarged by rotation (a factor favoring a fast redwards evolution, see Sect. 4) while the star on the whole is not too strongly mixed (a factor that would favor a blue position in the HR diagram). We then note that the impacts of the enhanced mass losses at the red supergiant stage are much stronger than for the non-rotating case. This comes from the fact that the cores are more massive and thus this favors at that stage a blue loop. Finally the last panel shows the situation for quite high initial velocities. In that case, the first crossing of the HR diagram is quite long because the stars are strongly mixed. Since the star becomes lately a red supergiant, any enhanced mass loss at that stage can only be applied during a short period. As a consequence the enhanced mass loss effects remain marginal.

These numerical simulations illustrate how mixing and mass loss can play together to enhance the blue loops or on the contrary for diminishing their importance. In the cases studied here, all the models finish their evolution with an
Effective temperature below 3.7, except the non rotating $25 \times \dot{M}$, which ends at an effective temperatures slightly higher, around 3.75. So all these models end their life as red supergiants\footnote{Note that the models were pursued until the end of the core He-burning phase and thus there may be still some changes in the HR position during the advanced phases. Due to the shortness of these phases, the positions indicated here should however not be too much altered unless very strong mass losses occur.}

7 The final fate

The chemical structures of a few representative models for a 15 M\(_\odot\) at solar metallicity are shown in Fig. 5. The left panel corresponds to the standard mass loss during the RSG phase. The results for all rotational velocities are similar. All these models end their life with a massive H-rich envelope comprising in all cases more than 5 M\(_\odot\). These models will likely produce type II-P supernovae and a neutron star. All the models with enhanced mass loss rates have structures similar to those in the middle and right panels. The mass has been strongly reduced, very high N/C ratio are obtained and only a very tiny H-rich layer still covers the surface. These models may explode as type II-P or II-L supernovae\footnote{Supernovae spectra should be computed to see which type will appear. Naively from the small mass of hydrogen, one would favor a type II-L supernova.}.
Interestingly one sees that there is no big changes between the 10 and 25×Ṁ models (and this remains true for whatever the rotation is). This is because when the mass loss rates are higher, the duration of the RSG phase is shortened. Thus at the end, all the models lose more or less the same amount of mass and end their lifetimes with quite similar structure. In Georgy et al. (2012), we suggested that, may be, stronger mass loss rates during the RSG phase could produce the very low luminous WC stars observed by Sander et al. (2012). The present calculations show that these WC stars cannot be produced from 15 M⊙ with enhanced RSG mass loss rates of up to 25 times the standard mass loss rates.
8 Conclusion

The main results of the above discussions are the following:

- Models of formation for a massive star like Betelgeuse through accretion indicate that the formation time is quite short (about 300 000 years which corresponds to 1-2% of the total lifetime). When rotation is accounted for during the accretion process, one obtains that such a star begins its evolution with a nearly flat rotation profile justifying the use of that approximation in most grids of stellar models published so far.

- The observations of the surface abundances and rotation allow to constrain the models provided single (or non interacting) stars with similar masses, metallicities are compared at same evolutionary stages (see Maeder et al. 2009).

- We discussed the main parameters influencing the duration of the first crossing of the HR diagram.

- The surface abundances given for Betelgeuse are in agreement with the predictions of models. It is however difficult to decide whether the progenitor of Betelgeuse was slowly or moderately rotating.

- We discussed the various evolutionary scenarios after the RSG phases and showed that 15 M$_\odot$ solar metallicity models, whatever the initial rotation between 0 and 0.7×$\upsilon_{\text{crit}}$, are distributed between two scenarios: 1) stars remaining a RSG star until the end of their lifetime; 2) blue loops occur but the star ends its stellar life as a red supergiant.

- Whatever the initial rotation between 0 and 0.7×$\upsilon_{\text{crit}}$ and the mass loss rate during the RSG phase between 1 and 25×$\dot{M}$, the supernova progenitor will be a RSG. There is no solution, changing the initial rotation and/or the mass loss rate during the RSG phase producing a WR star from a single 15 M$_\odot$ star.

Beside rotation and mass loss, other parameters may influence the evolution of stars, like the initial composition, the magnetic field and multiplicity. Let us just conclude by a question: one can wonder whether the surface magnetic field may have an impact on the slow wind of Betelgeuse. If we use the parameter $\eta = \frac{B^2/8\pi}{\rho\upsilon^2/2}$ giving the ratio of the energy density in the magnetic field to that of the kinetic energy of the wind (Ud-Doula et al. 2009), using the numerical values quoted in the introduction, we obtain a value $\sim 1$. Thus the magnetic field would just be strong enough to have some impact on the wind. It may for instance force the matter to follow the magnetic lines and thus extract angular momentum from the star. Such a magnetic braking may play some role in slowing down the star not only at the surface but also in more deeper regions. Also Thirumalai & Heyl (2012) find that the presence of a small magnetic field of about 1G is sufficient to
drive material from close to the stellar surface up and out of its gravity well, by means of a magneto-rotational wind.

References

Aurière, M., Donati, J.-F., Konstantinova-Antova, R., et al. 2010, A&A, 516, L2
Beech, M., & Mitalas, R. 1994, ApJS, 95, 517
Behrend, R., & Maeder, A. 2001, A&A, 373, 190
Bernasconi, P. A., & Maeder, A. 1996, A&A, 307, 829
Brott, I., Evans, C. J., Hunter, L., et al. 2011, A&A, 530, A116
Chieffi, A., & Limongi, M. 2013, ApJ, 764, 21
Ekström, S., Meynet, G., Chiappini, C., Hirschi, R., & Maeder, A. 2008, A&A, 489, 685
Ekström, S., Georgy, C., Eggenberger, P., et al. 2012, A&A, 537, A146
Georgy, C. 2012, A&A, 538, L8
Georgy, C., Ekström, S., Meynet, G., et al. 2012, A&A, 542, A29
Giammone, P. 1967, Zeitschrift für Astrophysik, 65, 226
Groh, J. H., Meynet, G., & Ekström, S. 2013, A&A, 550, L7
Harper, G. M., Brown, A., & Guinan, E. F. 2008, AJ, 135, 1430
Kuiper, R., Klahr, H., Beuther, H., & Henning, T. 2010, ApJ, 722, 1556
Lambert, D. L., Brown, J. A., Hinkle, K. H., & Johnson, H. R. 1984, ApJ, 284, 223
Langer, N. 2012, ARAA, 50, 107
Lauterborn, D., Refsdal, S., & Weigert, A. 1971, A&A, 10, 97
Le Bertre, T., Matthews, L. D., Gérard, E., & Libert, Y. 2012, MNRAS, 422, 3433
Maeder, A. 1987, A&A, 178, 159
Maeder, A., & Meynet, G. 2001, A&A, 373, 555
Maeder, A., & Meynet, G. 2012, Reviews of Modern Physics, 84, 25
Maeder, A., Meynet, G., Ekström, S., & Georgy, C. 2009, Communications in Astero-seismology, 158, 72
Perrin, G., Ridgway, S. T., Coudé du Foresto, V., et al. 2004, A&A, 418, 675
Przybilla, N., Firnstein, M., Nieva, M. F., Meynet, G., & Maeder, A. 2010, A&A, 517, A38
Renzini, A., Greggio, L., Ritossa, C., & Ferrario, L. 1992, ApJ, 400, 280
Salasnich, B., Bressan, A., & Chiosi, C. 1999, A&A, 342, 131
Sander, A., Hamann, W.-R., & Todt, H. 2012, A&A, 540, A144
Stancliffe, R. J., Chieffi, A., Lattanzio, J. C., & Church, R. P. 2009, PASP, 26, 203
Thirumalai, A., & Heyl, J. S. 2012, MNRAS, 422, 1272
Ud-Doula, A., Owocki, S. P., & Townsend, R. H. D. 2009, MNRAS, 392, 1022
Uitenbroek, H., Dupree, A. K., & Gilliland, R. L. 1998, AJ, 116, 2501
Vanbeveren, D., De Donder, E., van Bever, J., van Rensbergen, W., & De Loore, C. 1998, New Astronomy, 3, 443
Yoon, S.-C., & Cantiello, M. 2010, ApJL, 717, L62
Yorke, H. W., & Bodenheimer, P. 2008, Massive Star Formation: Observations Confront Theory, ASP Conf. Ser. 387, 189