Charming charm, beautiful bottom and quark–gluon plasma in the Large Hadron Collider era

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After a few microseconds of the creation of our Universe through the Big Bang, the primordial matter was believed to be a soup of the fundamental constituents of matter – quarks and gluons. This is expected to be created in the laboratory by colliding heavy nuclei at ultra-relativistic speeds. A plasma of quarks and gluons, called quark–gluon plasma (QGP) can be created at the energy and luminosity frontiers in the Relativistic Heavy Ion Collider, at Brookhaven National Laboratory, New York, USA, and the Large Hadron Collider at CERN, Geneva, Switzerland. Heavy quarks, namely the charm and bottom quarks, are considered as novel probes to characterize QGP, and hence the produced quantum chromodynamics matter. Heavy quark transport coefficients play a significant role in understanding the properties of QGP. Experimental measurements of nuclear suppression factor and elliptic flow can constrain the heavy quark transport coefficients, which are key ingredients for phenomenological studies, and they help to disentangle different energy loss mechanisms. We give a general perspective of the heavy quark drag and diffusion coefficients in QGP and discuss their potentials as probes to disentangle different hadronization mechanisms, as well as to probe the initial electromagnetic fields produced in non-central heavy-ion collisions. Experimental perspectives on future measurements are discussed with special emphasis on heavy flavours as the next-generation probes in view of new technological developments.

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to be the primordial matter formed at the infancy of our universe, just a few microseconds after the creation of the universe through the Big Bang. This primordial matter of quarks and gluons, because of its large concentration of energy and high temperature, expands with time (like an expanding fireball) through various complex processes. These processes include formation of composite hadrons from quarks and gluons called hadronization (corresponding to a system temperature, which marks the quark-hadron phase transition: deconfinement transition); chemical freezeout, where the particle abundances are frozen (inelastic collisions stop) and kinetic freeze-out (ceasing of elastic collisions), followed by free streaming of the secondary particles to reach the detectors found around the interaction point of the hadronic/nuclear collisions in the experimental area. The study of the properties of QGP is a field of high contemporary interest and remarkable progress has been made in the last decades towards understanding the properties of strongly interacting QGP. In this article, we focus on heavy flavour particles as a powerful probe of this primordial matter and their enriched measurements at the LHC energies given the high luminosity and detector upgrade programmes with high-end technologies.

Figure 2 is a pictorial representation of three generations of quarks and their masses. The masses of charm and bottom quarks are higher than up, down and strange quarks, which are taken as LQs (flavours). Although charm, bottom and top are considered as heavy quarks (HQs), because of the huge mass of top quarks and their low production cross-section, they are not considered for the present discussions. HQs mainly charm and bottom quarks, because of their large masses are considered as novel probes to characterize the properties of the QGP phase. These HQs are created in hard processes which are accessible to perturbative QCD (pQCD) calculations. Therefore, their initial distribution is theoretically known and could be verified by experiments. They are produced in the early stages of collisions and witness the entire space–time evolution of the created fireball and can act as an effective probe of the created QCD matter. HQs as coloured objects interact strongly with the plasma constituents and their momentum spectra are strongly modified. This is expressed by the nuclear suppression factor, $R_{AA}(p_T)$, ratio of the measured HQs momentum spectra ($\text{yields}$) in nucleus–nucleus to proton–proton collisions, rescaled by the number of binary collisions. If there were no interactions with QGP (as well as no cold nuclear matter effects like shadowing), one would indeed find $R_{AA} = 1$. Another observable is the elliptic flow, $v_2(p_T) = \langle \cos(2\Phi) \rangle$ of HQs. Here $\Phi$ is the azimuthal angle of emission of the secondary particles in hadronic/nuclear collisions. It is a measure of anisotropy in the angular distribution of the produced heavy mesons as a response to the initial anisotropy in coordinate space in non-central nucleus–nucleus collisions, transferred by the bulk to the HQs.

The relaxation time ($\tau_{HQ}$) of a HQ of mass $M$ at a temperature $T$ is larger than that of light partons by a factor of $M/T (> 1)$. In other words, the light quarks and gluons get thermalized faster than HQs. The propagation of HQs through QGP can therefore be treated as interactions between equilibrium and non-equilibrium degrees of freedom. The Fokker–Planck (FP) equation provides an appropriate framework for such processes.

Several theoretical studies have been made on various observables like $R_{AA}$ and $v_2$ of HQs within FP and the relativistic Boltzmann approach, which are then confronted with the experimental measurements. The HQs drag ($\gamma$) and momentum diffusion coefficients ($D_p$) are the key inputs to solve the FP equation, in order to study the momentum evolution of HQs in QGP medium to compute its $R_{AA}$ and $v_2$, which contain the microscopic details mentioning how HQs interact with the hot QGP medium. HQ drag coefficient is responsible for its energy loss, while the diffusion coefficient is responsible for its momentum broadening. The drag and diffusion coefficients of HQs can be computed starting from the HQ–LQ scattering matrix element. The HQs drag and momentum diffusion coefficients are related through the fluctuation–dissipation relation.
several studies in which non-perturbative effects have been incorporated. In the recent past, a simultaneous description of both energy-loss mechanisms is a major challenge to all the theoretical models and is known as the 'heavy quark puzzle'. Before the first experimental observations, it was expected that interaction of HQs with QGP could be characterized by pQCD, which led to the expectations of a smaller modification of their spectra and a smaller $v_2$. However, the first observations of non-photonic electrons coming from heavy meson decays measured at the highest RHIC energy have shown a surprisingly large modification of their spectra and a quite large $v_2$, indicating strong interactions between HQs and the QGP medium. This is substantially beyond the expectations from pQCD interactions. These observations have triggered several studies in which non-perturbative effects have been incorporated. In the recent past, a simultaneous study of both the observables, $R_{AA}(p_T)$ and $v_2(p_T)$, has received significant attention, as it has the potential to constrain the temperature dependence of HQ transport coefficients in the QGP medium and disentangle different energy-loss mechanisms. Recent studies based on temperature and momentum dependence of transport coefficients and Bayesian model to data analysis have obtained similar conclusions from different viewpoints.

Interestingly, the origin of $v_2$ is different for HQs than the bulk matter. The bulk develops its $v_2$ from the combined effect of the initial coordinate space anisotropy created in non-central collisions and interaction among the quarks and gluons which constitute the bulk. However, HQs develop a substantial part of $v_2$ due to their interactions with the bulk medium and partly from the light partons as a consequence of hadronization. A coupled study of light and heavy particle flow harmonics in heavy-ion collisions on event-by-event basis is another interesting topic. Experimental measurements in this direction will offer further novel insights on HQ – bulk in-medium interaction and the temperature dependence of HQ transport coefficients.

Figure 3 shows the variation of HQ $D_{v}$. A standard quantification of the space diffusion coefficient is done in terms of a dimensionless quantity, obtained from different models in comparison with the lQCD results. Being a mass-independent quantity, it can provide a general measure of the QCD interaction. Additionally, this quantity can be calculated within the framework of lQCD, being directly related to the spectral function. This highlights HQs as a probe of QGP, which have the potential to link the phenomenology constrained from the experimental data to lQCD for studying the transport properties of the hot QCD matter. Energy loss experienced by energetic partons leads to a suppression of final hadrons with high momentum, known as jet quenching. At high momentum, one can extract the HQ jet quenching parameter, the average transverse momentum broadening squared per unit length, which contains information regarding jet–medium interactions.

Once the temperature of the system goes below the quark–hadron transition temperature, HQs convert to hadrons through hadronization. The hadronization dynamics plays an important role in determining the final momentum spectra and therefore, $R_{AA}$ and $v_2$ in both LQ and HQ sectors. In particular, for HQs, it is generally expected that a coalescence mechanism is in action, especially in the low and intermediate momentum. Heavy baryon to heavy meson ratios ($\Lambda_c/D$ and $\Lambda_c/B$), are considered fundamental for the understanding of in-medium hadronization. Furthermore, the heavy baryon to meson ratio can serve as a tool to disentangle different hadronization mechanisms.

With the advent of very high-energy accelerators like those at RHIC and LHC, we are able to create extremely strong magnetic fields in non-central heavy-ion collisions. The estimated values of the initial magnetic field strengths ($10^{19}$ Gauss) are several orders of magnitude higher than those predicted at the surface of magnetars.

Figure 3. Spatial diffusion coefficient as a function of scaled-temperature obtained within different theoretical models to describe experimental data, along with the results from lQCD. Here, $T_c$ is the critical temperature for a quark–hadron transition.
This is the highest ever produced magnetic field on the earth created by human beings. However, the magnetic field strength rapidly decreases as two ions recede from each other. However, this remains much stronger than the critical field (Schwinger field) during the lifetime of the created fireball. Since HQs are produced at the early stages of heavy-ion collisions, their dynamics will be affected by such a strong magnetic field. They will also be able to retain these effects till their detection as open heavy flavours like D mesons in experiments. HQ directed flow $v_1$ is identified as a novel observable to probe the initial electromagnetic field produced in high-energy non-central heavy-ion collisions. The sign of the directed flow for a charged particle will be opposite to its antiparticle mainly due to the response of opposite charges to the electromagnetic field. The recent LHC measurements, along with the RHIC findings, on the D-meson $v_1$, give indications of the strong electromagnetic field produced in high-energy heavy-ion collisions. It must be mentioned that the magnitude of the HQ directed flow at LHC energy is about 1000 times larger than that of LQs. This is mainly because HQs are produced in the early stages of collisions and hence witness the peak of the electromagnetic field. Furthermore, HQs, due to their large relaxation time in comparison to LQs, are capable of retaining the memory of the initial non-equilibrium dynamics more effectively. Hence they carry a stronger signal of the early electromagnetic fields. Further, the momentum anisotropy present in the QGP medium can induce Chromo–Weibel (The Weibel instability is a plasma instability present in the electromagnetic plasmas, which arises when the momentum distribution of the charged particles is anisotropic. The non-abelian analogue of the Weibel instability is termed as Chromo–Weibel instability, which also follows from anisotropy in the momentum space.) instability. The impact of anisotropy on HQ transport is significant compared to the case when HQs are moving in an isotropic QGP medium. Non-perturbative effects on HQ transport coefficients near $T_c$ play a significant role. To describe both $R_{AA}$ and $v_2$ simultaneously, the inclusion of non-perturbative effects is essential.

As mentioned before, HQs are produced in the very early stages of heavy-ion collisions due to their large masses. Hence, they can probe the pre-equilibrium phase which is produced before the formation of QGP. The effect of the pre-equilibrium phase might be more significant for low-energy heavy-ion collisions. For example, in the case of $Au+Au$ collisions at RHIC energy, results based on event simulation show that equilibration is achieved approximately within 1 fm/c. Whereas the lifetime of the QGP phase is about 5 fm/c. Hence the lifetime of the out-of-equilibrium phase is approximately 20% of the total lifetime of QGP. Currently, HQs are also used as a tool to probe the glasma, the strong gluon field produced in the early stages of high-energy heavy-ion collisions.

On the experimental front, there have been several measurements on heavy-flavour spectra, nuclear modification factor, elliptic and directed flow in proton–proton and heavy-ion collisions. However, going to lower transverse momentum and dealing with signal-to-background ratio has been a challenge so far, because of technological limitations. On the contrary, the future is more exciting because ALICE, which is a dedicated experiment for studying QGP, has entered into detector upgrades with gas electron multiplier-based time projection chamber to deal with high-multiplicity and high-luminosity, the inner tracking system (ITS) with lower material budget to enhance the signal-to-background ratio and detection efficiency at lower transverse momenta. As the lifetimes of heavy flavours are very less, their decay lengths ($\ell = \frac{m}{c^2}$, $c$ is the speed of light in vacuum and $r$ is the lifetime of the particle in its local rest frame) are small. Hence they decay close to the interaction vertex by creating a secondary vertex. This necessitates tracking devices closer to the interaction point with less material budget to reduce the detection background. To have a better grasp, for instance, the innermost silicon tracker of the CMS experiment at the LHC is at 33 mm distance from the interaction point and the ALICE ITS is 39 mm from the interaction point. Due to the high mass, all the heavy flavours decay before reaching the detectors, and their detection is based on the invariant mass reconstruction, where one encounters high background from the combinatorics (daughters from other sources and material interactions). This makes the experimental studies of heavy flavours a highly complex endeavour.

To overcome these problems, the LHC upgrade plans with the next level of technology are highly encouraging. ALICE – the dedicated experiment at the LHC to study the primordial matter – QGP has planned for the installation of ITS3 (the third generation inner tracking system) in LHC long shutdown-3 (LS3). This will have a novel vertex detector consisting of three curved wafer-scale ultra-thin silicon monolithic pixel sensors arranged in perfectly cylindrical layers (Figure 4). This will have an unprecedented low material budget of 0.05% $X_0$ ($X_0$ is called radiation length and is the mean path length (g cm$^{-2}$) required to reduce the energy of an electron by the factor $1/e$ (energy loss through Bremsstrahlung – depends on atomic number and atomic mass of the material)) per layer, with the innermost ITS layer positioned at only 18 mm radial distance from the interaction point. This upgrade is expected to overcome the present limitations in terms of proper identification of secondary vertices, efficiency at low $p_T$, and dealing with signal-to-background ratio to a greater extent. For a quantitative understanding, Figure 5 shows an expected order of magnitude better signal-to-background ratio in the detection of $\Lambda^+_c$, compared to ITS2 (which is being installed during the ongoing long shutdown-2). This will help with the higher detection efficiency of particles containing HQs,
opening a new domain of QCD studies. In view of the LHC plan for dedicated high-multiplicity proton–proton (pp) runs, the future directions of research and the search for QGP droplets in high-multiplicity pp collisions remain exciting with HQs as potential probes24.

Beyond the energy reach of the present LHC, the planned Future Circular Collider at CERN is expected to collide proton on proton at a centre-of-mass energy of 100 TeV and heavy-ion collisions at 39 TeV per nucleon with a circumference of 100 km, compared to 27 km of the LHC25. This new energy and luminosity frontier would facilitate the study of signals of the early universe in proton–proton and heavy-ion collisions with a variety of new observations, with special emphasis on heavy-flavours. This article gives the theoretical and experimental status of characterization of primordial matter – QGP using heavy flavours as a potential probe. Future research in this direction with improved technologies and energy/luminosity would help in resolving many theoretical issues and for a better understanding of the QCD matter formed in high-energy collisions.

Readers not familiar with the subject of QGP may refer to Sahoo and Nayak26.

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