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Bidirectional switching assisted by interlayer exchange coupling in asymmetric magnetic tunnel junctions

D. J. P. de Sousa,1,* P. M. Haney,2 D. L. Zhang,1 J. P. Wang,1,† and Tony Low1,‡

1Department of Electrical and Computer Engineering,
University of Minnesota, Minneapolis, Minnesota 55455, USA
2Physical Measurement Laboratory, National Institute of Standards and Technology, Gaithersburg, Maryland 20899-6202, USA
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We study the combined effects of spin transfer torque, voltage modulation of interlayer exchange coupling and magnetic anisotropy on the switching behavior of perpendicular magnetic tunnel junctions (p-MTJs). In asymmetric p-MTJs, a linear-in-voltage dependence of interlayer exchange coupling enables the effective perpendicular anisotropy barrier to be lowered for both voltage polarities. This mechanism is shown to reduce the critical switching current and effective activation energy. Finally, we analyze the possibility of having switching via interlayer exchange coupling only.

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Magnetic tunnel junctions (MTJs) that can be switched bidirectionally by electrical means are highly desirable for low power consumption applications[1]. Current-induced magnetization reversal is one of the most promising and reliable technologies available for achieving bidirectional switching in MTJs[2–5].

Current-induced switching relies on spin transfer torque (STT), where the interaction between current-carrying spins which are misaligned with the magnetization leads to magnetic dynamics and reversal[4]. In addition to STT, a charge current modifies the interlayer exchange coupling (IEC) between fixed and free layers via an additional field-like torque[5–7]. Though frequently called “field-like spin transfer torque component”, in this work we refer to this torque component as interlayer exchange torque[6]. Denoting the free (pinned) magnetic layer orientation by \( \mathbf{m} (\mathbf{m}_p) \) [See inset Fig. 1(a)], the total current-induced torque density is

\[
\mathcal{N} = T_{IEC} \mathbf{m} \times \mathbf{m}_p + T_{STT} \mathbf{m} \times (\mathbf{m} \times \mathbf{m}_p). \tag{1}
\]

Unlike in spin valves where the IEC torque is negligible, it has been demonstrated that \( T_{IEC} \) is comparable to \( T_{STT} \) in MgO-based MTJs, considerably affecting the magnetization dynamics of the free layer[8–10]. However, while the importance of \( T_{STT} \) for magnetization switching is well understood, the contribution of \( T_{IEC} \) is often omitted in many analyses and poorly explored.

For perpendicular MTJs (p-MTJs), the critical switching current \( J_c \) is directly proportional to the total effective perpendicular anisotropy \( K_{eff} \)[11, 12]. Such proportionality reflects the fundamental problem encountered in memory technology, where one seeks to improve \( K_{eff} \) for better retention of information while reducing the critical switching current \( J_c \) for low-power consumption[12]. Particularly, the voltage control of magnetic anisotropy (VCMA) is currently being quoted as one of the most promising methods to circumvent this problem, as it provides a mechanism to reduce the anisotropy barrier \( K_{eff} V \), where \( V \) is the volume of the free layer, only when a voltage is applied across the MTJ, enabling one to reduce \( J_c \) momentarily while maintaining a sizeable \( K_{eff} \) at zero applied voltage[12–15]. However, while it can reduce the critical switching current for a given applied voltage by reducing \( K_{eff} \), it tends to increase \( K_{eff} \) for the opposite voltage polarity. The ability to overcome the anisotropy barrier bidirectionally while decreasing the critical current density is highly desirable, and remains a long-standing goal in the search for low power consumption spintronics.

In this work, we show that \( T_{IEC} \) can assist STT switching by effectively reducing the anisotropy barrier for both voltage polarities in asymmetric p-MTJs. We demonstrate that \( T_{IEC} \) directly competes with the total effective intrinsic uniaxial anisotropy quantified by \( K_{eff} \), enabling one to reduce the critical switching current bidirectionally by tuning the degree of asymmetry of the p-MTJ. Our model includes the combined effects of STT, VCMA and IEC effects on p-MTJs, which are all known to be present in this kind of system[12, 16].

The total torque acting on the magnetization vector of the free layer is decomposed into different contributions, as given by the Landau-Lifshitz-Gilbert (LLG) equation[17]

\[
\frac{d\mathbf{m}}{dt} = -\gamma \mathbf{m} \times \mathbf{H}_{eff} + \alpha \mathbf{m} \times \frac{d\mathbf{m}}{dt} + \frac{\gamma}{\mu_0 M_{S\text{free}}} \mathcal{N}, \tag{2}
\]

where \( \mathbf{m} = \mathbf{M}/M_S \), with \( \mathbf{M} \) being the magnetization of the free layer with saturation \( M_S \), \( \gamma \) is the gyromagnetic ratio, \( \alpha \) is the intrinsic damping parameter, \( \mu_0 \) is the vacuum permeability and \( t_{\text{free}} \) is the thickness of the free layer. The effective field is \( \mathbf{H}_{eff} = (2K_{eff}(V)m_z/\mu_0 M_S)\mathbf{z} \), with \( \mathbf{z} \) being the axis perpendicular to the free layer plane and \( m_z \) being the \( z \) component of \( \mathbf{m} \). The total effective anisotropy coefficient is given by \( K_{eff}(V) = K_{eff}(0) + \xi V \) with \( K_{eff}(0) = K_i/t_{\text{free}} = \mu_0 M_S^2/2 \) being the effective perpendicular magnetic anisotropy at zero voltage with interfacial anisotropy \( K_i \). The VCMA coefficient is \( \xi \) and \( V \) the applied voltage across the p-MTJ. We assume
order in \(V\). Our convention for the voltage is that \(V > 0\) leads to an electron flow from the fixed layer to the free layer. For symmetric p-MTJs, \(T_{\text{IEC}}\) is an even function of applied voltage, i.e., the spatial top-bottom symmetry requires that \(C_1 = 0\) and \(C_2 \neq 0\)[19]. In this case, one can solve Eq. (3) analytically for \(V_c\) to find
\[
V_c = \frac{2a\xi}{\beta\Delta} T_{\text{IEC}}(0)m_z (1 + \alpha C_1/\beta_{\text{STT}})^{-1},
\]
where we have assumed \(\xi = 0\), i.e., no VCMA effect, and neglected terms of order \(\alpha^2\). Interestingly, Eq. (4) shows that \(V_c\) does not depend on \(C_2\) in this limit. Hence, this result is consistent with the fact that \(T_{\text{IEC}}\) has little or no influence on the magnetization switching in conventional symmetric p-MTJs.

The situation for asymmetric p-MTJs is different. In this case, theoretical[7, 20] and experimental[21] analysis have shown that \(C_1 \neq 0\), giving a sizable linear voltage-dependent contribution to \(T_{\text{IEC}}\). In this situation, \(T_{\text{IEC}}\) acts like a torque due to an effective field with sign determined by \(V\) and direction aligned with the magnetization of the fixed layer. For a given applied voltage \(V\), this results in an unidirectional anisotropy, to be contrasted with the intrinsic uniaxial magnetic anisotropy. We explore the consequences of this symmetry breaking induced contribution by assuming, for simplicity, \(\xi = 0\) and \(C_2 = 0\). Equation (3) can then be easily solved:
\[
V_c = \frac{2a\xi}{\beta_{\text{STT}}} T_{\text{IEC}}(0)m_z (1 + \alpha C_1/\beta_{\text{STT}})^{-1},
\]
where \(V_c\) is reduced by a factor of \(1 + \alpha C_1/\beta_{\text{STT}}\). This simple analysis shows the relevance of \(T_{\text{IEC}}\) in reducing the critical switching current. A comparison between experiments from Refs. [8, 21] indicates that \(C_1 = 0\) and \(C_1 \approx 30\) kA/m for symmetric and asymmetric CoFeB/MgO/CoFeB MTJs, respectively. These results show the possibility of tuning \(V_c\) via \(C_1\).

The above analysis, albeit qualitative, demonstrates the possibility of reducing critical switching voltage when \(T_{\text{IEC}}\) exhibits strong asymmetric dependence on voltage, i.e., \(C_1 \gg 0\). According to Eq. (5), the sign of \(C_1/\beta_{\text{STT}}\) must be positive in order to decrease the \(V_c\). While \(\beta_{\text{STT}}\) is usually positive, it was experimentally observed that one can tune the sign and magnitude of \(C_1\) by controlling the relative composition between fixed and free magnetic layers[21]. In the following section, we first evaluate the voltage modulation of both \(T_{\text{STT}}\) and \(T_{\text{IEC}}\) within a single orbital quantum transport model and explore the dependence of the critical current density with p-MTJ asymmetry.

**Non-equilibrium torques.** In the absence of spin-orbit coupling[22], the torque exerted on the magnetization of the \(i\)-th atomic plane of the free layer is related to the spin current flux into that plane as \(T_i = -\nabla \cdot Q_i = Q_{i-1,i} - Q_{i,i+1}\) where \(Q_{i,j}\) is the spin-current density between atomic planes \(i\) and \(j\). The total torque exerted on the semi-infinite magnetic lead reads \(T = \sum T_i = \ldots\).
that the ratio $C_1/\beta_{\text{STT}}$ is positive if one choose $\delta > 0$.

**Critical current density.** The critical current density $J_c$ is computed by computing the current-voltage relation using Landauer’s formula and non-equilibrium Green’s function. This relation enables the previously computed voltage-dependent $T_{\text{IEC}}$ and $T_{\text{STT}}$ to be converted to their corresponding current-dependent. Figure 2(a) shows $J_c$ as a function of the asymmetry parameter $\delta$ for P to AP (red circles) and AP to P (blue triangles) switching with $K_i \approx 1.3 \text{ mJ/m}^2$ and VCMA coefficient $\xi = 20 \text{ kJ/V}^2\text{m}^2$. The result clearly shows that $J_c$ decreases with asymmetry, which can be interpreted as follows: The presence of $T_{\text{IEC}}$ in asymmetric p-MTJs reduces $K_{\text{eff}}$ for both voltage polarities, as qualitatively described by Eq. (5). Therefore, the effective energy barrier between P and AP configurations decreases and less current is necessary for magnetization reversal.

The symmetry breaking also has important consequences for thermally activated switching. Following Ref. [28], we have derived expressions for the effective activation energy in the presence of $T_{\text{IEC}}$:

$$E_{\text{eff}}^b = E_{\text{anis}} \left(1 - \frac{T_{\text{STT}}}{T_{\text{IEC}}}\right) \left(1 - m_z \frac{T_{\text{IEC}}}{2T_{\text{STT}}} K_{\text{eff}}\right), \quad (7)$$

where one can extract the switching time $\tau^{-1} = f_0 \exp(-E_{\text{eff}}^b/k_BT)$, with $f_0$ being an attempt frequency. The anisotropy energy barrier $E_{\text{anis}}(V) = K_{\text{eff}}(V)\xi V$ quantifies the thermal stability factor $\Delta = E_{\text{anis}}(0)/k_BT$. Figure 2(b) shows the voltage dependence of the normalized effective energy barrier $E_{\text{eff}}^b/E_{\text{anis}}$ for P to AP ($V > 0$) and AP to P ($V < 0$) switching considering several different asymmetry parameters $\delta$. In this plot we use the voltage dependence of non-equilibrium torques from the quantum transport model. As one can see, the activation energy drops faster with $V$ for asymmetric p-MTJs, allowing for higher switching probabilities at a given temperature $T$.

**Switching by voltage control of IEC.** So far, we have shown that in asymmetric p-MTJ, $T_{\text{IEC}}$ can assist STT switching by effectively reducing the anisotropy barrier
for both voltage polarities. Anisotropy and voltage dependent IEC torques can be written as derivatives of an effective energy, given by:

$$E(\theta) = K_{\text{eff}} \sin(\theta)^2 + (T_{\text{IEC}}/t_{\text{free}}) \cos(\theta),$$  \hspace{1cm} (8)

where $\theta$ is the angle between $\mathbf{m}$ and $\mathbf{m}_p$. Stable equilibrium points are found at energy minima, where the total field-like torque vanishes.

Figures 3(a) and (b) show the energy landscape for negative and positive current-density of $J = 5 \times 10^7 \text{A/cm}^2$ for different p-MTJ asymmetries. We have also plotted the energy at zero applied voltage in black solid lines for comparison purposes. One sees that $K_{\text{eff}}$ alone gives rise to two metastable equilibrium configurations with P ($\theta = 0$) or AP ($\theta = \pi$) alignment, emphasizing the axial nature of perpendicular anisotropy.

Figure 3(a) shows the angular dependence of the total energy for different asymmetries $\delta$ at applied $V < 0$. For the symmetric case ($\delta = 0$ eV), a negative bias voltage gives rise to a negative $T_{\text{IEC}}$ [See Fig. 1(c)] while decreasing $K_{\text{eff}}$. The associated energy landscape for this case is shown as a dashed blue curve in Fig. 3(a). One sees that the stability of the P (AP) configuration is enhanced (suppressed) due to the unidirectional nature of the IEC torque. The dotted olive curve in Fig. 3(a) shows the angular dependence of energy for the same current density considering an asymmetric p-MTJ with $\delta = 0.6$ eV. In this case, the previously metastable AP configuration is now a maximum, indicating a current-induced instability and subsequent switching from $\theta = \pi$ to $\theta = 0$.

The dash-dotted red curve shows that the effect is even more pronounced if one further increases the asymmetry to $\delta = 1.8$ eV.

For $V > 0$, $K_{\text{eff}}$ now increases with $V$. For symmetric p-MTJs, $T_{\text{IEC}}$ is an even function of the bias and, therefore, remains negative with positive applied voltage [See Fig. 1(c)]. The resulting energy landscape is represented by the dashed blue curve in Fig. 3(b), where one observes an even greater stability in the P configuration, increasing the difficulty to switch from P to AP. In asymmetric p-MTJs, however, $T_{\text{IEC}}$ changes sign under reversal of the voltage polarity. Such behavior results in the curves corresponding to $\delta \neq 0$ eV in Fig. 3(b). In these cases, the P (AP) configuration tends to become more unstable (stable) as one increases the asymmetry, favoring P to AP switching. In particular, the case $\delta = 1.8$ eV shows that one can completely destabilize the P configuration, showing pure IEC bidirectional bipolar switching.

Conclusions. We have studied the simultaneous impact of VCMA, IEC and STT for p-MTJs. We demonstrated that for asymmetric devices, linearly varying $T_{\text{IEC}}$ plays an important role in STT switching by renormalizing the effective anisotropy barrier. Such effect leads to reduced critical switching current for magnetization reversal, and can even lead to switching based on IEC alone.

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* Electronic address: sousa020@umn.edu
† Electronic address: jpwang@umn.edu
‡ Electronic address: tlow@umn.edu
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