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Evaluation of Vibration Analysis to Assess Bone Mineral Density in Children

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Abstract
The effectiveness of vibration analysis to assess bone mineral density (BMD) in children with suspected reduction in bone density was studied. A system was designed that measured the ulna's vibration responses in vivo. The system was evaluated on the ulnae of 48 children (mean age=12.0, std=3.5 years), 31 of whom had been confirmed to have osteogenesis imperfecta (OI). All children had dual energy X-ray absorptiometry (DXA) scan as part of their routine clinical care and vibration analysis was performed on the same day. Frequency spectra of the ulnae's vibration responses were obtained and processed by principal component analysis. Four main principal components were selected and together with age, sex and right hand ulna's length were used in a regression analysis to estimate BMD. Regression analysis was repeated using the children's leave-one-out and partitioning methods. The percentage similarity and correlation between the DXA-derived and vibration analysis estimated BMDs using the leave-one-out were 80.34% and 0.59 and for partitioning were 74.2% and 0.64 respectively. There was correlation between vibration analysis BMD readings and those derived from DXA however a larger study will be needed to better establish the extent to which vibration analysis can assist in assessing bone density in clinical environments.

Keywords Bone mineral density. Vibration analysis. Osteogenesis imperfecta

1 Introduction
The bones in a skeletal structure provide support, help with movement, protect vital internal organs and maintain mineral homeostasis and acid base balance. They are a reservoir of growth factors and cytokines and provide the environment for hematopoiesis within the marrow spaces [1]. Bone is a composite material that is made up of osteoblasts and osteocytes (for supporting cells), osteoclasts (for remodeling cells) and non-mineral matrix of collagen and non-collagenous proteins called osteoid, with inorganic mineral salts deposited within the matrix [2]. Assessing bone mineral density (BMD) in children is important for diagnosing and treating conditions that weakens its strength thus leading to frequent fractures. Bone mass gained during childhood and adolescence is an important factor in influencing the risk of developing osteoporosis later in life. Peak bone mass, i.e. the amount of bony tissue accrued at the end of skeletal maturation [3], is dependent on several factors including genetic, weight-bearing physical activity, nutrition and hormonal status. A number of hereditary or acquired disorders may result in reduced bone density and thus increased bone fragility in children. Osteogenesis imperfecta (OI) is probably the commonest genetic cause and refers to a group of disorders associated with recurrent fractures, low bone mass and skeletal fragility [4-6]. Other causes of low bone mass in children include chronic inflammatory conditions (e.g. juvenile idiopathic arthritis, Crohn's disease), immobility (e.g. Duchene muscular dystrophy, cerebral palsy) and drugs (e.g. steroids, anti-epileptics).

Methods of assessing bone density include conventional radiographs, computed tomography (CT), quantitative CT (QCT), peripheral quantitative CT (pQCT) and high-resolution peripheral quantitative CT (HRpQCT), magnetic resonance imaging (MRI), quantitative ultrasound (QUS), single X-ray absorptiometry (SXA) and dual X-ray absorptiometry/dual energy X-ray absorptiometry (DXA/DEXA) [7]. Medical imaging using magnetic resonance imaging (MRI) and CT are the most useful diagnostic modalities as they may provide further anatomical and pathological/diagnostic information [8]. DXA is the most commonly used non-invasive technique to quantify bone mass (BM) and BMD [7,9]. It has however a number of limitations when it is applied to growing individuals, as the major changes in skeletal size and mass taking place with growth may result in incorrect interpretation of results [9,10]. Furthermore, although DXA is a relatively low exposure technique, children with suspected low bone mass often have repeated imaging, therefore a non-ionizing radiation technique, even as a screening tool would be beneficial in reducing the amount of radiation that these children are exposed to.

Vibration analysis is a well-established technique in industry for analyzing physical structural properties of materials including their densities. There were a number of encouraging reports of vibration analysis to assess bone integrity [11-19]. These were mainly in vitro on adults, but our study has been conducted in children in vivo and the vibration analysis and DXA derived BMD results have been compared.
2 Methodology

In this section the procedures to recruit the patients, the manner their bone vibration signals were recorded and processed are explained.

2.1 Recruitment

This was a prospective observational study conducted between August 2016 and August 2017. Ethical approval for the study was obtained from the National Health Service (UK) Ethics Committee. Forty eight children and young people aged between 5 and 18 years (mean 12 years, standard deviation 3.5 years), attending the Radiology Department of a single pediatric tertiary referral center for a DXA scan to assess bone density were prospectively consented and recruited. Their relevant clinical and demographic details are summarized in Table 1.

Table 1 Summary of participants' clinical and demographic details

| Variable                  | Parameters | Values                      |
|---------------------------|------------|-----------------------------|
| Age (years)               | Mean (SD)  | 12.0 (3.5)                  |
|                           | Median     | 11.9                        |
|                           | Minimum    | 5.8                         |
|                           | Maximum    | 17.3                        |
|                           | Range      | 11.5                        |
| Sex                       | Male (%)   | 24 (50%)                    |
|                           | Female (%) | 24 (50%)                    |
| Whole body BMD (g/cm²)    | Mean (SD)  | 0.69 (0.16)                 |
|                           | Median     | 0.68                        |
|                           | Minimum    | 0.44                        |
|                           | Maximum    | 1.05                        |
|                           | Range      | 0.61                        |
| Weight (kg)               | Mean (SD)  | 41.3 (19.5)                 |
|                           | Median     | 35.9                        |
|                           | Minimum    | 15.1                        |
|                           | Maximum    | 120.1                       |
|                           | Range      | 105.0                       |
| Height (cm)               | Mean (SD)  | 141.6 (18.4)                |
|                           | Median     | 144.0                       |
|                           | Minimum    | 90.0                        |
|                           | Maximum    | 175.4                       |
|                           | Range      | 85.4                        |
| Right hand ulna length (cm)| Mean (SD)  | 21.5 (3.3)                  |
|                           | Median     | 21.5                        |
|                           | Minimum    | 15.5                        |
|                           | Maximum    | 28                          |
|                           | Range      | 12.5                        |
| Confirmed medical diagnosis| None       | 2                           |
|                           | Osteogenesis imperfecta | 31                           |
|                           | others      | 15                          |

DXA scans were performed by radiographers within the hospital's Radiology Department using a fan-beam GE Lunar iDXA densitometer and following the standard protocols [20]. All DXA scans were clinically indicated and none were performed solely for the purposes of this study. Following their DXA scan, the recruited children and their parents/guardians completed the vibration test assent or consent forms (depending on their age) prior to the children having the bone vibration test. Vibration analysis was conducted on all children by a single individual on the same day as the DXA scan.

2.2 Bone vibration recording system and its set up

The ulna was chosen for bone density assessment because of its relative ease for both inducing and measuring vibration. The olecranon was avoided as it is a more sensitive part of the ulna. Vibration was induced by tapping the ulna two centimetres away from the olecranon. The vibration response was recorded from the head of the ulna at the point where the ulna is most prominent (closest to the skin surface). The vibration tests were performed using a computer controlled system shown in Fig. 1. It consisted of: (i) a bone vibration inducing device (called a tapper), (ii) a circuit driver for the tapper, (iii) a vibration response sensor, (iv) a signal conditioning (amplification and filtering) device, (v) an analogue to digital convertor (called myDAQ©) and (vi) a computer for the graphic user interface, storage and analysis facilities. The individual parts are described in the next sections.

Fig. 1 Bone vibration response recording system

2.3 Bone vibration inducing system

A small computer controlled device (called a tapper) was designed to induce bone vibration in vivo. The device has an embedded moving steel shaft that moves forward and then returns to its rest position. To activate the tapper, a square pulse was sent from the computer through the National Instrument© data acquisition device (myDAQ©) to a power transistor acting as an interface to the tapper. The transistor ensured sufficient current to drive the device. The device was placed gently on the required test site (two centimetres from the olecranon) and the shaft of the tapper mildly tapped the skin surface above the bone with a controlled force, inducing the required bone vibration. The force magnitude and duration were controlled by varying the magnitude and duration of the supply voltage to the device. A user interface based on the National Instrument’s LabView© fully controlled the tapper’s operation. The tapper's supply voltage was 10 volts and each tap lasted for 50 ms. The exerted force and the duration of each tap were adjusted through the graphic user interface developed in the National Instrument’s LabView©. For each child, 10 bone
vibration responses were recorded each separated by one second. Prior to using the device on children, its operation was tested on healthy adult volunteers and its parameters (magnitude of the force and duration of each tap) were established in such a way as to provide a sufficiently large vibration response signal without causing discomfort. At the start of each recording, the children were informed that they could immediately stop the recording if they felt uncomfortable, but none of the children indicated they felt any discomfort.

The induced bone vibration responses were detected using a CM-01B\textsuperscript{©} vibration sensor [21] that was fully encapsulated in a customized plastic casing to ensure electrical safety for the purpose of this study. The sensor is a contact microphone device that uses sensitive but robust PVDF piezoelectric film combined with a low-noise electronic preamplifier for vibration detection. Its sensitivity is 40 volts/mm with flat frequency response in the range of 8 Hz to 2 kHz. Its electronic noise is 1 mV (peak-to-peak). We did not use inertia measurement units (e.g. accelerometer and gyroscope) for vibration detection as these could detect hand movements, a recognized problem for in vivo studies, especially those involving children. The used sensor’s advantage was that it did not pick up body movements. The sensor was fixed on the skin above the ulnar head using Mefix\textsuperscript{©} self-adhesive fabric.

The vibration signal was amplified by a factor of 6 and then lowpass filtered using a 4\textsuperscript{th} order Butterworth filter with a cut-off frequency set to 2 kHz. The cut-off frequency was the bandwidth limit of the vibration sensor. The signal was then digitized using the National Instrument’s myDAQ\textsuperscript{©} data acquisition device. The sample rate was 100,000 samples per second (the limit of myDAQ). The myDAQ was connected to a laptop computer using a USB cable that displayed the bone vibration responses in real-time and stored them for off-line processing.

The graphic user interface was developed using the National Instrument’s LabView\textsuperscript{©} software. It enabled real time display of signals, allowed the user to adjust the amplitude and width of the square pulse that activated the tapper thus controlling the tapping force, the duration of each tap, time between successive taps and sample rate.

2.4 Bone vibration recording procedure

The vibration signals were recorded with the patient sitting on a chair of adjustable height with their right hand resting on a suitably located soft mat on a table. The vibration was induced by gently holding the tapper on the skin, 2 cm from the olecranon. The computer then facilitated the sending of 10 pulses to the tapper, recording 10 successive vibration responses separated by 1 second. Following the vibration test, the child was asked for feedback regarding the comfort of vibration compared with DXA by completing a non-validated questionnaire.

2.5 Bone vibration processing procedure

The steps to process the vibrations signals are explained in the following sections.

**Feature extraction and selection:** The vibration signals each consisting of 10 vibration responses had their mean removed and were discrete Fourier transformed prior to obtaining their magnitude spectra. The magnitudes of the peaks in the frequency magnitude spectra declined sharply at around 300 Hz. There were 20 peaks up to 300 Hz and these magnitudes were chosen as features for analysis. These gave sufficient spectral information without producing an excessive number of variables. The resulting magnitudes were normalized by initially dividing them by the value of the largest peak (this ensured a maximum magnitude of 1, with all others values in relation to 1) and then they were divided by their standard deviations. This normalization ensured that spectral features across the children could be better compared. The 20 selected normalized magnitudes were processed by principal component analysis (PCA) and a scree plot of the Eigen values was obtained. This indicated that the four main principal components represented 90.2\% of the overall variance. Therefore the vibration signal for each child was represented by four main principal components. Age and sex can influence BMD values and ulna (right ulna’s length was measured for all children) length (\(u\)) could affect the acquired vibration responses, these three parameters were also included in the feature matrix, thus providing seven features in total (in this matrix females and males were represented numerically by 0 and 1 respectively).

**Estimating BMD using vibration analysis:** Linear regression was used to model the bone vibration information as indicated by

\[ \begin{bmatrix} pc_{11} & pc_{12} & pc_{13} & pc_{14} & u & age_i & sex_i \\ pc_{21} & pc_{22} & pc_{23} & pc_{24} & u & age_i & sex_i \\ . & . & . & . & . & . & . \\ pc_{n1} & pc_{n2} & pc_{n3} & pc_{n4} & u & age_i & sex_i \end{bmatrix} \begin{bmatrix} c_1 \\ c_2 \\ . \\ . \\ c_7 \end{bmatrix} = \begin{bmatrix} BMD_1 \\ BMD_2 \\ . \\ . \\ BMD_n \end{bmatrix} \]  

where \(n\) is the number of children, \(pc_{ik}\) is the \(k\)\textsuperscript{th} principal component for child \(i\) (\(i=1...n\)), \(age_i\) and \(sex_i\) are age and sex for child \(i\), \(c_1...c_7\) are the regression coefficients and \(BMD_i\) is the DXA derived BMD for \(i\)\textsuperscript{th} child. The regression modelling required the coefficients \(c_1...c_7\) to be determined. As the data set was not large, two approaches were followed for comparison. In the first method, referred to in this paper as, “leave-one-out”, the feature matrix (on the left hand side of equation (1)) and the BMD matrix (on the right hand side equation (1)) indicating DXA derived BMD values for all but one child were formed. Using the two matrices, the regression coefficients were determined. The coefficients were then multiplied with the feature matrix of the excluded child, i.e.

\[ [pc_{\text{excluded}}, pc_{\text{excluded}}, pc_{\text{excluded}}, u_{\text{excluded}}, age_{\text{excluded}}, sex_{\text{excluded}}] \]

to estimate the vibration analysis derived BMD. The excluded child was returned to the matrices and the process was repeated for all children. For the second regression modelling method, referred to in this paper as the “partition method”, the feature matrix and DXA derived BMD matrix were formed for all 48 children and then arranged in ascending order of BMD values. The children in the odd rows of the matrices were used to determine the regression coefficients. The coefficients were then applied to the children in the even rows of the matrices to estimate vibration analysis BMD values for those children. The sorting operation ensured roughly equal distribution of BMD values in determining the regression coefficients and
in evaluating the method. The vibration derived BMD values estimated using regression analysis were compared with those derived from DXA.

3 Results

The distribution of whole-body BMD values provided by DXA for the children included in the study is shown in Fig. 2. The largest proportion of BMD values was at 0.6 g/cm$^2$. Although density is conventionally measured as mass per volume with the unit of g/cm$^3$, DXA derived BMD is represented as mass per unit area, i.e. g/cm$^2$, and so the unit of g/cm$^2$ is used for BMD representation throughout this paper.

Fig. 2 Distribution of DXA derived BMD values for children included in the study.

Fig. 3 shows a typical vibration response for the ulna. Its oscillation lasts about 70 ms. The amplitude of the response is initially relatively large but decays very rapidly. The initial response has a narrow width (higher frequency) with duration about 5 ms.

Fig. 3 A typical vibration response recorded from an ulna.

Given that the vibration was both induced in and recorded from the ulna through skin, (and potentially fat and muscle), a key concern was the extent to which these soft tissues as well as the device inducing the vibration and the vibration sensor would alter the recorded vibration responses. As the recordings were performed in vivo on children, detailed exploration of these factors was not practical in this study. However, we have previously explored these issues in vitro using turkey legs [22, 23]. In these studies, vibration responses were recorded from intact turkey legs (i.e. with all soft tissues left in place) and then the experiment was repeated with the bones completely stripped of all soft tissues. Our results indicated that although soft tissue alters the recorded vibration response’s shape and oscillation frequency, the vibration response recorded from the skin surface still correlated with that recorded directly from the bone’s surface. In this current study, vibration was induced and vibration response recorded very close to the ulna (through a few millimetres of skin thickness) in an attempt to minimize the damping effect of soft tissues.

Fig. 4 Magnitude frequency spectrum of an ulna’s vibration response.

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Fig. 4 shows the vibration response magnitude frequency spectrum recorded from a child's ulna. The magnitude frequency spectra of the recorded vibration responses showed some variations from child to child with regards to the shape, magnitude and frequency range, but their main frequency components were below 300 Hz.

Fig. 4 Magnitude frequency spectrum of an ulna’s vibration response.

Fig. 5 shows the scree plot of the Eigen values of the principal components used to decide on number of components for regression analysis. The first four principal components were chosen as they amounted to 90.2% of overall Eigen value (latent).

Fig. 5 The scree plot of the principal components.

Figs. 6a and b show the relationship between the DXA derived BMD values and the BMD values estimated using vibration analysis using leave-one-out and partition methods respectively. Figure 6a includes all children but Figure 6b contains the 24 children included in the evaluation matrix of the regression model. The figures indicate that there is a relationship between the DXA derived and vibration analysis estimated BMD values, although there are significant deviations between the two measures for some children.
Fig. 6 Correlation between DXA derived and vibration analysis estimated BMDs (a) leave-one-out method and (b) partition method.

Figs. 7a and b show bar charts for DXA derived and vibration analysis estimated BMD values using the leave-one-out and partition methods. The BMD differences between the DXA and vibration analysis are shown in Fig. 8.

Some children had significantly larger deviation between their DXA derived and vibration analysis estimated BMD values. This issue was further explored by considering the cases that had at least 30% deviation. The associated children were 2, 4, 8, 10, 15, 16, 28, 37, 39, 47 and 48 (the child numbers associate with Figure 7a). The related information such as medication, previous history of bone fractures, height, weight and body mass index (BMI) for these 11 children were compared against the remaining 37 children. Amongst these, the BMI for the 11 children showed a noticeable difference compared to other 37 children. The analysis results are summarized in Table 2. The BMI for the 11 children was 23.87 kg/m$^2$ while the other 37 children this was 18.5 kg/m$^2$. BMI represents the weight (kg)/ height$^2$ (m$^2$). A BMI of 25.0 kg/m$^2$ or higher is overweight while 18.5 to 24.9 kg/m$^2$ is not overweight. This analysis results may suggest that the vibration analysis method may be less accurate in children with a higher BMI. This may be due to a larger damping effect of soft tissues on recorded bone vibration responses.

Fig. 7 BMD bar chart for (a) leave-one-out method, (b) partition method. Red: DXA derived, Green vibration analysis estimated.

Fig. 8 Differences between the DXA derived and vibration analysis estimated BMD, (a) leave-one-out method, (b) partition method.
Table 2 Body mass index (BMI) analysis

| Children                      | Weight average (standard deviation) (kg) | Height average (standard deviation) (m) | BMI average (standard deviation) (kg/m²) |
|-------------------------------|-----------------------------------------|----------------------------------------|-----------------------------------------|
| 2, 4, 8, 10, 15, 16, 28, 37, 39, 47 and 48 (subject numbers are as those in Fig. 7a) | 48.95 (30.34)                          | 1.38 (0.21)                            | 23.87 (9.77)                            |
| Remaining 37 children         | 39.09 (14.07)                           | 1.43 (0.18)                            | 18.50 (3.95)                            |

Box plots of DXA derived and vibration analysis estimated BMD values for leave-one-out and partition regression analysis methods are shown in Figs. 9a and b. The vibration analysis estimated BMD values have a broader distribution than DXA derived BMD values but their medians are close.

![Box plots of DXA derived and vibration analysis estimated BMD values](image)

Fig. 9 Box plots of BMD values obtained using (a) leave-one-out method, (b) partition method.

In order to allow clinicians to compare two different measurement techniques, an analysis based on the Bland-Altman statistical method was used [24]. The analysis is based on a scatter plot of the difference of two techniques against their averages. The Bland-Altman plot for the DXA derived and vibration analysis estimated methods using leave-one-out method is shown in Fig. 10(a) and for the partition method in Fig. 10(b). The plots indicate the bias, i.e. average difference. This should ideally be zero. They also indicate the limits of agreement, i.e. a range that spans BMD difference from mean-1.96 \* standard deviation to mean+1.96 \* standard deviation. This range represents 95% of comparison points. For the leave-one-out method the limits of agreement were from -0.3 to 0.36 g/cm² and for the partition method the limits were from -0.4 to +0.49 g/cm².

![Bland-Altman plot](image)

Fig. 10 Bland-Altman plot for (a) leave-one out and (b) partition methods.

Table 3 compares the vibration analysis estimated BMD values for both leave-one-out and partition methods against the DXA derived BMD values.

Table 3 Comparison of BMD (g/cm²) values obtained from DXA with those estimated from vibration analysis (VA) for the leave-one-out and partition methods.

| Statistics                  | Leave-One-Out | Partition |
|-----------------------------|---------------|-----------|
| DXA                         | VA            | DXA       | VA         |
| Minimum                     | 0.44          | 0.16      | 0.45       | 0.04       |
| Maximum                     | 1.05          | 1.17      | 1.05       | 1.22       |
| Range                       | 0.61          | 1.01      | 0.60       | 1.18       |
| Mean                        | 0.69          | 0.66      | 0.70       | 0.66       |
| Standard-deviation          | 0.16          | 0.20      | 0.16       | 0.29       |
| Median                      | 0.68          | 0.66      | 0.69       | 0.70       |
| Interquartile-range         | 0.20          | 0.23      | 0.20       | 0.40       |

The mean BMD values for both leave-one-out and partition methods (vibration analysis) differ from the mean...
DXA derived BMD values by 4.35% and 5.71% respectively. The respective medians differ by 2.94% and 1.45%. Therefore the vibration analysis and DXA give close mean and median values for BMD. The BMD range (maximum - minimum BMD values), standard deviation and interquartile range for vibration analysis are larger than those for DXA derived values. The standard deviation of BMD values for the leave-one-out and partition methods (vibration analysis) differ from the standard deviation of DXA derived BMD values by -25.00% and -81.25% respectively. The 11 children with much larger BMI could be causing the large differences in the range and standard deviation.

Summary statistics comparing DXA derived and vibration analysis estimated BMD values for the leave-one-out and partition regression analysis methods are provided in Table 4.

**Table 4** Summary statistical comparison of the methods for determining BMD

| Method           | Correlation coefficient | Percentage similarity |
|------------------|-------------------------|-----------------------|
| Leave-one-Out    | 0.59                    | 80.34                 |
| Partition        | 0.64                    | 74.20                 |

The correlation coefficients between the DXA derived and vibration analysis estimated BMD values for the leave-one-out and partition methods were 0.59 and 0.64 respectively. The percentage similarity (ps) (indicated in Table 4) were also calculated using

\[ ps = \left(1 - \sum_{i=1}^{n} \left( \frac{\text{abs}(d_i - v_i)}{d_i} \right) \right) \times 100 \]  

where n is the number of children (n=48 for leave-one-out and 24 for partition method) and \(d_i\) and \(v_i\) are DXA derived and vibration analysis estimated BMD values for child i.

The value for \(ps\) indicates average similarity between the DXA derived and vibration analysis estimated BMD values. The \(ps\) values for the leave-one out and partition methods were 80.34% and 74.20% respectively.

4 Discussion

The study indicates that vibration analysis may have potential to be a harmless, non-invasive, cost effective and easy to apply method for estimating BMD. However a number of issues need to be further studied before vibration analysis can be used as a routine BMD assessment method in the clinical environment. These include:

- The number of children included in the study was small. This could have reduced the accuracy of the vibration analysis method in determining BMD when using the regression model. The BMD values estimated using vibration analysis relied on regression modelling. An increase in the number of children can provide a more representative range of BMD values and thus could improve its performance.

- Partitioning and leave-one-out methods were compared in setting up the regression models. In both models, DXA derived values were used as reference. The DXA derived values may have inaccuracies as discussed in the introduction of the paper. It would be advantageous to calibrate the regression models against other imaging modalities particularly High-Resolution Peripheral Computed Tomography (HRpQCT). However there is a cost implication for research for the scans as well as ethical issues related subjecting children to the scans for the purpose of research. We are currently synthesising bones with varied densities and will test the vibration analysis on these artificial bones.

- The instrumentation system used in the study to record the vibration responses is currently a prototype and its operation can be further improved. The current device is hand held and the manner in which it was held in relation to the recording site for each patient may have affected the resulting responses. In this study all vibration responses were recorded by a single experienced operator thus reducing this effect. She initially practiced the device on adult volunteers to obtain best operating performance. We are currently building a new version of the device that can make the device operator independent.

- The analysis was performed only on the ulna. We will in future repeat the tests on other long bones such as the tibia and fibula to ascertain the degree to which their vibration derived BMD measurements correlate with those obtained from the ulna.

- The effects of soft tissue, muscle and joints on the recorded vibration responses were not incorporated in the analysis. Modelling could be made more sophisticated by incorporating these effects.

- The study indicated that the vibration analysis may not be as effective in children with high BMI. This issue needs a more detailed investigation with a larger number of children.

- The effects of medication and previous history of ulna fractures on results were not explored in this study (due to small sample size) and thus can be explored further.

The vibration analysis method is not designed to be a replacement for DXA or any other modality for BMD assessment but rather it is aimed to be a cost effective, easy to use, non-invasive and completely harmless technology for screening purposes. Our study supports previous related studies indicating the potential of vibration analysis in assessing bone density. As DXA and other modalities for assessing BMD are expensive and require access to specialized medical expertise and centres, the vibration analysis approach may allow medical practitioners to have a practical tool for a quick screening of those suspected of abnormal bone density, resulting in an increased likelihood of earlier detection of osteoporosis and its medical treatment resulting in a reduction in bone fractures. Furthermore, the tool may allow the BMD improvement resulting from medications to be monitored more regularly as it is a harmless and cost-effective tool.

5 Conclusion

An *in vivo* evaluation of vibration analysis to estimate bone mineral density (BMD) in 48 children with suspected low bone mass including some with known
osteogenesis imperfecta (OI) was carried out. Two regression models were set up based on data partitioning and leave-one-out approaches. DXA derived BMD values were used as reference. The DXA derived and vibration analysis estimated BMD values correlated, indicating that vibration analysis may be valuable in assessing BMD. We are currently further developing both the instrumentation and data processing of the bone vibration analysis method to improve its accuracy and reliability.

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