Rare top quark decays at a 100 TeV proton–proton collider:
\( t \rightarrow bWZ \) and \( t \rightarrow hc \)

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Abstract We investigate extremely rare top quark decays at a future proton–proton collider with centre-of-mass energy of 100 TeV. We focus on two decay modes: radiative decay with a \( Z \) boson, \( t \rightarrow bWZ \), and flavour-changing neutral decay with a Higgs boson, \( t \rightarrow hc \), the former being kinematically suppressed with a branching ratio of \( \mathcal{O}(10^{-6}) \) (Altarelli et al., Phys Lett B 502:125–132, 2001), and the latter highly loop-suppressed, with a branching ratio of \( \mathcal{O}(10^{-15}) \) (Aguilar-Saavedra, Acta Phys Polon B 35:2695–2710, 2004). We find that \( t \rightarrow bWZ \) will be very challenging to observe in top quark pair production, even within well-motivated beyond-the-standard model scenarios. For the mode \( t \rightarrow hc \) we find a stronger sensitivity than that obtained by any future LHC measurement by at least one order of magnitude.

1 Introduction

The top quark’s large mass suggests that it may be intimately-connected to the mechanism of electroweak symmetry breaking (EWSB). Furthermore, it is unique as a colour-charged particle because of the fact that it decays before hadronizing. The top quark decays mostly through the channel \( t \rightarrow bW \) with much smaller contributions from other SM processes. The QCD production of top quarks at the Large Hadron Collider (LHC) is expected to be high, with \( \sigma(pp \rightarrow t\bar{t}) \approx 950 \text{ pb} \) at 14 TeV centre-of-mass energy [3], and would be 40 times larger at a proton collider with a centre-of-mass energy of 100 TeV (e.g. the Future Circular hadron hadron Collider – FCC-hh [4,5]). Given its large production rates, the top quark provides simultaneously interesting tests of QCD (through its production mechanisms) and of electroweak physics (through its decay channels). The Tevatron has already measured several properties of the top following its discovery, and the LHC is already adding further precision measurements. The purpose of the present study is to investigate to which extent a FCC-hh can provide valuable information to our knowledge of the top quark properties and couplings. Here, we focus on the potential for the observability of the radiative SM decay mode, \( t \rightarrow bWZ \), and on the decay of the top quark through the direct interaction between the top and charm together with the Higgs boson, i.e. \( t \rightarrow hc \).

The decay of the top quark to a bottom quark, a \( Z \) and a \( W \) boson, \( t \rightarrow bWZ \), received some attention 20 years ago, with several studies addressing its rate and potential sensitivity to new physics [1,6–9]. A peculiar feature of this process is that it occurs near the kinematical threshold: \( m_t \approx m_b + m_W + m_Z \) and is thus suppressed within the Standard Model (SM), predicted to be \( \mathcal{O}(10^{-6}) \). In the studies of Refs. [1,6,8], it was pointed out that one has to take into account the finite widths of the \( Z \) and \( W \) bosons when calculating this decay mode. Indeed, if the widths are ignored, the current particle data group nominal values [10] of the particles involved: \( m_t \approx 173.1 \text{ GeV}, m_b \approx 4.18 \text{ GeV}, m_Z \approx 91.19 \text{ GeV} \) and \( m_W \approx 80.39 \text{ GeV} \) would imply \( m_t < m_b + m_W + m_Z \) and would suggest a kinematically-forbidden decay. Nevertheless, if the gauge boson widths are properly taken into account the decay can proceed. This leads to \( \mathcal{O}(10^4) \) top quark pair production events containing the decay during the lifetime of the high-luminosity LHC (HL-LHC) with an integrated luminosity of 3000 fb\(^{-1}\), inclusively over the decays of the \( Z \) and \( W \) bosons. Consequently, the process will likely be impossible to observe at the LHC. However, given the substantial increase in cross section at the FCC-hh this channel is expected to yield \( \mathcal{O}(10^6) \) events, justifying a more detailed investigation into its observability.

Flavour-changing neutral (FCN) decays of the top quark appear at one loop and have a strong suppression due to the Glashow–Iliopoulos–Maiani (GIM) mechanism and second-
third generation mixing [2,11,13,14]. Within the SM, this suppression leads to the following branching ratios: \( \text{BR}(t \rightarrow \gamma c) \sim 10^{-14}, \text{BR}(t \rightarrow gc) \sim 10^{-12}, \text{BR}(t \rightarrow Zc) \sim 10^{-14} \) and \( \text{BR}(t \rightarrow hc) \sim 10^{-15} \) [2], rendering them unobservable at the current and future colliders. Consequently, the measurement of such processes within current capabilities would clearly signal the presence of BSM phenomena. Here, we focus on the transition \( t \rightarrow hc \), where the new physics effect is treated as an effective interaction between the top quark, the charm quark and the Higgs boson.

This paper is organised as follows: in Sect. 2 we consider theoretical aspects of the \( t \rightarrow bWZ \) decay and construct a simple phenomenological analysis to assess its observability at the FCC-hh within the SM. To complement this analysis, we study the allowed size of an enhancement to the decay rate due to the presence of a charged heavy scalar boson contribution, given current experimental constraints. Subsequently, in Sect. 3, we analyse the decay \( t \rightarrow hc \), taking into account the effective coupling \( h-tc \) and extract a bound by looking at a clean final state at the FCC-hh, with \( h \rightarrow \gamma\gamma \). Finally, we present our conclusions in Sect. 4.

2 Top quark decays to \( bWZ \)

2.1 Theoretical considerations

2.1.1 Defining the final state

The ‘cleanest’ channels in which the process \( t \rightarrow bWZ \) contributes are those containing multiple leptons. Here we will focus on the cases \( t \rightarrow be^+\nu_e\mu^+\mu^- \) and \( t \rightarrow bj\mu^+\mu^- \), which receive contributions from other intermediate states in addition to \( t \rightarrow bWZ \). We examine the observability of these processes by looking at the particle content in the final states only and we do not attempt to separate the \( t \rightarrow bWZ \) contribution.\(^1\)

In Ref. [1], the ratio \( R = \text{BR}(t \rightarrow b\nu_e\mu^+\mu^-)/[\text{BR}(W \rightarrow \mu
u_\mu) \times \text{BR}(Z \rightarrow \nu\nu)] \) was considered as a definition of the process \( t \rightarrow bWZ \). Taking into account that the top quarks are on-shell, we can use an equivalent definition:

\[
R' = \frac{\text{BR}(pp \rightarrow t\bar{t} \rightarrow (b\mu^+\nu_\mu)\bar{v})}{\text{BR}(pp \rightarrow t\bar{t} \rightarrow (b\mu^+\nu_\mu)\bar{v}) \times \text{BR}(Z \rightarrow \nu\nu)}.
\]  \( (1) \)

We have calculated \( R' \) by using the \texttt{MG5\_aMC@NLO} Monte Carlo event generator [15,16]. Within the given errors, the results for \( R' \) are in good agreement with those for the ratio \( R \) appearing in the third column of Table 2 of Ref. [1]. To make a direct comparison, we show the results in Table 1.

\(^1\) This separation is not possible due to interference of the \( t \rightarrow bWZ \) contribution with other diagrams.

| \( m_t \) (GeV) | \( R' \) | \( R \) (Ref. [1]) |
|----------------|---------|-----------------|
| 170            | 1.55 \times 10^{-6} | 1.53(4) \times 10^{-6} |
| 171            | 1.62 \times 10^{-6} | – |
| 172            | 1.71 \times 10^{-6} | – |
| 173            | 1.79 \times 10^{-6} | – |
| 174            | 1.89 \times 10^{-6} | – |
| 175            | 2.00 \times 10^{-6} | 1.96(5) \times 10^{-6} |

**Table 1** The ratio of branching ratios defines the \( t \rightarrow bWZ \) as described in the main text. The results of Ref. [1] are only provided in 5 GeV intervals.

![Graph](image-url)

**Fig. 1** The decay width of the process \( t \rightarrow be^+\nu_e\mu^+\mu^- \) for \( m(\mu^+\mu^-) > 70 \) GeV at leading order and next-to-leading order in QCD as a function of the bottom quark mass. The lower inset shows the ratio of NLO to LO where we have used the values of the masses and constants given in Table 1 of Ref. [1].

2.1.2 Next-to-leading order corrections

Since the decay process occurs close to the top mass threshold, it is interesting to investigate the impact of next-to-leading order (NLO) QCD corrections. To consider a scenario which might be realistic in a phenomenological study, we examine corrections to the decay process \( t \rightarrow be^+\nu_e\mu^+\mu^- \), with the invariant mass of \( \mu^+\mu^- \) pair taken to lie above 70 GeV to remove the photon contribution, \( \gamma \rightarrow \mu^+\mu^- \).

We use \texttt{MG5\_aMC@NLO} to calculate the SM decay width, \( \Gamma \), setting \( m_t \) = 173 GeV and varying the bottom mass between 0.2 and 5.2 GeV. In Fig. 1 we show the variation of the decay width as a function of the input bottom mass. In addition, we also present the ratio between the NLO and the leading order (LO) corrections in the lower inset. It is evident that the NLO corrections reduce the branching ratio by about 10%. The impact of increasing the \( b \)-quark mass is larger at NLO...
than at LO, which is due to the phase space becoming even more restricted close to the top mass threshold. Given the null results of the phenomenological analyses (see below), we do not consider higher-order corrections in more detail.

2.2 Phenomenological analysis for $t \to bWZ$

We construct a simple phenomenological analysis to determine whether a FCC-hh at 100 TeV will be sensitive to the SM top radiative decay $t \to bWZ$. We focus on the final states that arise through top pair production that contain one “signal” top decaying into 3 leptons and the other top decaying fully hadronically, i.e.

$$pp \to t\bar{t} \rightarrow (b\ell^+\nu_\ell^+\ell^-)(\bar{b}jj),$$

and its charge-conjugate, where $j$ is any light-flavour jet. In addition we also consider the case where one of the top quarks decays to oppositely-charged leptons and the other to only hadronic products:

$$pp \to t\bar{t} \rightarrow (bjj\mu^+\mu^-)(\bar{b}jj).$$

In our analysis, the jet reconstruction is done using the fastjet package [17, 18]. We simulate the signal and backgrounds using MG5_aMC@NLO [19–23] for the parton shower and non-perturbative effects, general-purpose Monte Carlo event generator HERWIG 7 for the shower and non-perturbative effects, such as hadronization and multiple-parton interactions.

2.2.1 The three-lepton final state

As a starting point for the analysis of the three-lepton final state:

$$pp \to t\bar{t} \rightarrow (b\ell^+\nu_\ell^+\ell^-)(\bar{b}jj),$$

we ask for two opposite-sign same-flavour leptons and one additional lepton, with $p_T > 20$ GeV within a pseudorapidity of $|\eta| < 6$. Furthermore, we ask that the oppositesign same-flavour leptons reconstruct the $Z$ mass, $m_{\ell^+\ell^-} \in [89, 93]$ GeV. As before, jets are reconstructed with the anti-$k_T$ algorithm with $R = 0.3$ and we demand that they satisfy $p_T > 20$ GeV within $|\eta| < 6$. Two of these jets are $b$-jet candidates. Here we assume that $b$-jets can be tagged with 100% efficiency, so as to give an upper estimate of the sensitivity to the processes under consideration. We then find the best combination of two or three jets that reconstruct the top quark mass by looking at all the combinations of jets. We call this combination the “reconstructed hadronic top” and require $m_{t,\text{reco}} \in [153, 193]$ GeV. We also ask that the distance $\Delta R$ between the sub-leading $b$-jet and the reconstructed $Z$ boson is $\Delta R < 1.0$.

Using the assumption that the missing transverse momentum is primarily due to the undetected neutrino from the “signal” top quark decay and using the mass-shell condition $m_T^2 = (p_T + p_T^L + p_T + p_T^L + p_T^Z)^2$ we obtain a quadratic equation, and hence two solutions, for the $z$-component of the neutrino momentum. We use these solutions to reconstruct two corresponding values of the total invariant mass momenta of the reconstructed top quarks. We require that both of these values lie within [350, 700] GeV.

To assess the detection prospects of this process we consider the background arising from $pp \to t\bar{t}Z$, where all three particles are taken to be on-shell in this case. Using the aforementioned basic cuts, and the LO cross sections for the signal, $\sigma_{\text{signal}} \simeq 3.0 \times 10^{-5}$ pb, and for the background contribution to the final state considered here (i.e. including branching ratios) $\sigma_{\bar{t}\bar{Z}} \simeq 0.10$ pb, we find an estimate of $\mathcal{O}(5)$ events for the signal and $\mathcal{O}(5000)$ events for the $t\bar{t}Z$ at an integrated luminosity of $10$ ab$^{-1}$, a ballpark estimate of the FCC-hh end-of-lifetime data sample. This implies that this channel will be impossible to observe during the FCC-hh lifetime, and we do not consider it here any further.

2.2.2 The two-lepton final state

To further investigate top quark radiative decays, let us now consider the signal process:

$$pp \to t\bar{t} \rightarrow (bjj\mu^+\mu^-)(\bar{b}jj).$$

As before, we consider only the main background channel: $pp \to t\bar{t}Z \rightarrow (bjj)(\bar{b}jj)(\mu^+\mu^-)$, where the pair of muons arises from the decay of an on-shell $Z$ boson. Our selection procedure focuses on the reconstruction of the top quark based on the combination of final state products ($bjj\mu^+\mu^-$). To reconstruct the $Z$ boson we require two oppositely-charged muons satisfying $|\eta| < 6$ such that the combined invariant mass is within the interval $[80, 100]$ GeV. We cluster final state particles, excluding the muons, with $p_T > 5$ GeV into anti-$k_T$ jets of $R = 0.3$. We require exactly two $b$-tagged jets. We then recluster the constituents of the $R = 0.3$ subjets into $R = 1.2$ “fat jets” using the anti-$k_T$ algorithm, excluding the previously $b$-tagged subjets. For each fat jet, we apply a mass drop algorithm as in Ref. [24] with parameters $\tau_{\text{cut}} = 1.5$ and $\mu = 0.25$. We determine the invariant mass $M'$ of the system composed by the pair of muons that reconstruct the $Z$ boson, the lowest $p_T$ $b$-tagged jet and the resulting subjet after the mass-drop application. The event is selected only if there is a fat jet such

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2 Charge-conjugate processes are taken into account from this point on by multiplying by the appropriate symmetry factors.

3 Defined as usual $\Delta R = \sqrt{\Delta \eta^2 + \Delta \phi^2}$, where $\eta$ is the pseudo-rapidity and $\phi$ is the azimuthal angle.

4 We employ this method to “groom” the jets, removing soft radiation.
that $140 \text{ GeV} < M' < 180 \text{ GeV}$ after the mass drop conditions are applied. Based on this selection we obtain the cross sections $\sigma_{\text{signal}} = 1.4 \times 10^{-4} \text{ pb}$ and $\sigma_{\text{background}} = 0.5 \text{ pb}$, for signal and background respectively, corresponding to a significance $S/\sqrt{B} = 0.6$ at an integrated luminosity of $10 \text{ ab}^{-1}$. Thus, it seems unlikely that this process would be detected in this channel.

2.3 Heavy charged Higgs bosons

The analyses of the previous sections indicate that the SM radiative decay of the top quark seems challenging to detect even at the 100 TeV FCC-hh. Nevertheless, one might ask whether it would be possible to observe an enhanced rate due to beyond-the-SM contributions. One possibility arises with the addition of a heavy charged Higgs boson, $H^\pm$ that couples to $W^\pm Z$ as well as top and bottom quarks. Such couplings have been probed in LHC experimental analyses, for example the ATLAS analyses at 8 TeV that appear in Refs. [25,26]. In Ref. [25], the process $gb \to H^- t \to (\bar{t}b)t$ (and charge conjugate) was searched for by the ATLAS experiment, using data corresponding to an integrated luminosity of $20.3 \text{ fb}^{-1}$. The diagram contributing to this channel, shown on the left in Fig. 2, has a rate that is directly proportional to the quartic power of the $H^\pm - t - b$ coupling. Similarly, in Ref. [26], the final state $H^\pm \to W^\pm Z$ was searched for using an equivalent dataset in vector boson fusion. The latter process, shown on the right in Fig. 2, has a rate proportional to the quartic power of the $H^\pm - W^\pm - Z$ coupling.

We simulate these two processes at LO using MG5_aMC@NLO and assume that the new scalar only possesses these two interactions. Hence, using the results obtained in the aforementioned articles [25,26], we derive constraints for the maximum and minimum allowed values of the decay width at LO. These are shown in Fig. 3. Evidently the enhancement factor is moderate over the range of scalar boson masses considered, with a maximal value of $\mathcal{O}(2)$ for a heavy charged Higgs boson mass of $\sim 200 \text{ GeV}$. Hence we can conclude that the addition of a heavy charged scalar cannot render this process observable at a 100 TeV collider. Note that due to the interference of the SM diagrams with the charged scalar diagrams, which can be negative, the decay width can possess values lower than those of the SM.

3 Top quark decays to Higgs boson-charm quark

3.1 The $h-t-c$ coupling

We now turn to the investigation of flavour-changing neutral decays of the top quark. We consider gauge-invariant and renormalizable Yukawa interactions of the form

$$\mathcal{L}_{thc} = \lambda_{ct}^h \bar{Q}_c H q_t + \text{h.c.},$$

(6)

where $Q_i$ is a left-handed doublet, $q_j$ is a right-handed singlet and $H$ is the SM Higgs doublet. We constrain our analysis to real and symmetric couplings: $\lambda_{ct}^h \equiv \lambda_{tc}^h = (\lambda_{ct}^h)^\dagger$.

Here we focus on the resulting top quark decay $t \to hc$, induced by couplings of the above kind. We also note that these couplings can lead to other interesting final states [27]. Various studies have already examined this process at the LHC [14,27,28], with the current best experimental constraint on $BR(t \to hc)$ at the LHC being 0.22% at 95% C.L., coming from ATLAS 13 TeV data (36.1 fb$^{-1}$) in the di-photon channel [29]. The corresponding best constraint at CMS is currently 0.47% through $h \to bb$ decays [31]. Naive extrapolation of the 13 TeV ATLAS result [29] to the high-luminosity LHC demonstrates that an integrated luminosity of 3000 fb$^{-1}$ implies an ultimate constraint of $BR(t \to hc) \lesssim 0.019\%$ through the $h \to \gamma\gamma$ channel alone. It is important to note here that the LHC analyses do not consider the tagging of charm jets in the derivation of

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5 This is obtained by extrapolating the number of events for the signal and backgrounds from 36.1 to 3000 fb$^{-1}$, assuming that the experimental details and analysis remain unchanged.

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these constraints. This implies that these limits are associated with the crucial assumption that the $t \to h u$ decay will be either absent or sub-dominant with respect to $t \to h c$. Alternatively, one can use these analyses to impose constraints on $t \to h u$, assuming $t \to h c$ is absent or sub-dominant.

In the present study we will analyse the prospect of constraining $\text{BR}(t \to h c)$ and $\lambda_{ht}^0$ through top quark pair production at the FCC-hh. To the best of our knowledge this represents the first estimate for a constraint on this coupling at the FCC-hh. Among all the decay channels, the one expected to provide the strongest contribution in the combination for the constraint is the one involving the transition $h \to \gamma \gamma$, and therefore we will focus on it in the present study. In our analysis we consider both the scenario with and that without charm-jet tagging, with values for the tagging efficiencies motivated by current LHC considerations [32].

### 3.2 Phenomenological analysis for $t \to hc$

We have implemented the interaction described by Eq. (6) in a UFO [33] model which we interface to MG5_aMC@NLO to generate signal $pp \to t \bar{t} \rightarrow (hc)t \bar{t}$ (and the charge-conjugate process) events. We also generate parton-level events for the backgrounds using MG5_aMC@NLO and perform shower and hadronization using HERWIG 7 as before. The background processes considered include those that include a Higgs boson in association with other particles: $pp \to t \bar{t} h$, $pp \to h jjW^\pm$ and those that contain non-resonant di-photon production: $pp \to t \bar{t} \gamma \gamma$, $pp \to \gamma \gamma jjW^\pm$, where the $W$ bosons were decayed to electrons or muons. Generation-level cuts were applied on the non-resonant photon samples: the photon transverse momentum was required to lie in $p_T > 10 \text{ GeV}$, the distance between two photons $\Delta R(\gamma, \gamma) > 0.1$ and the invariant mass of the two photons to satisfy $M_{\gamma \gamma} \in [110, 140] \text{ GeV}$. In all background samples we asked for the generation-level cuts on the jets and final-state leptons of $p_T > 20 \text{ GeV}$. The jets have been merged to the HERWIG 7 parton shower at tree level using the MLM method via the FxFx add-on module [34].

Our analysis is divided into two cases, either with the “non-signal” top decaying hadronically, $(t \to bjj)$ or semi-leptonically $(t \to b \ell \nu)$. The starting cross sections for both the hadronic and semi-leptonic final states, with the generation-level cuts described above, are given in the second column of Table 2. For the signal cross section we use a working value of $\lambda_{ht}^0 = 0.1$. To take into account higher-order effects and for the sake of simplicity, we have rescaled the leading-order cross sections for all processes by a $k$-factor of 2. This approximation does not have a significant impact on our derived constraints and can be fully addressed in a future analysis.

| Process | $\sigma^{\text{had}}_{\text{gen}}$ (pb) | $\sigma^{\text{f}}_{\text{gen}}$ (pb) |
|---------|-----------------|-----------------|
| $pp \to t \bar{t} \rightarrow (hc)t \bar{t}$ | 0.332 | 0.122 |
| $pp \to t \bar{t}h$ | 0.044 | 0.030 |
| $pp \to h jjW^\pm$ | 0.022 | 0.070 |
| $pp \to t \bar{t} \gamma \gamma$ | 0.042 | 0.028 |
| $pp \to \gamma \gamma jjW^\pm$ | 1.294 | 0.424 |

7 In general charm-jet tagging is currently less developed than $b$-jet tagging, see e.g. [32] for single-prong charm-jet tagging algorithm and [35] for a double-charm-jet tagger used in the context of Higgs searches.

8 As discussed in, e.g., [36], better forward detector coverage for $b$-jet or photon identification, up to $|\eta| \sim 3 - 3.5$ may increase signal efficiency at a future 100 TeV collider. In the present analysis we chose to be conservative, allowing identified objects only within $|\eta| < 2.5$. 

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Further details on the usage of this module for tree-level merging will be available in a future release of the HERWIG 7 manual.
due to the missing neutrino and reconstruct its $z$-component by solving the quadratic equation $m_W^2 = (p_t + p_\nu)^2$, where $p_t$ and $p_\nu$ represent the 4-momenta of the hardest lepton and the missing neutrino respectively. Here, we take $m_W = 80.4$ GeV. We then ask for one of the two solutions to reconstruct the top mass when combined with the $b$-jet within the range $[150, 200]$ GeV. In the hadronic top case we consider the invariant mass of combinations of the $b$-jet with one or two light jets and find the one closest to the top mass, taking $m_{\text{top}} = 173$ GeV. We then ask for this to lie in the same range: $[150, 200]$ GeV.

We summarise the main features of the analysis in Table 3. The resulting event yields after applying the analyses are shown in Tables 4 and 5 for the cases with and without charm tagging, respectively, at an integrated luminosity of $\mathcal{L} = 10$ ab$^{-1}$.

3.3 Constraints for $t \to hc$

To take into account the effect of the presence of systematic uncertainties, we assume that they only affect the total number of background events, $B$, by introducing a systematic uncertainty $\Delta B = \alpha B$, with $\alpha \geq 0$ parameterising the effect. We add this in quadrature to the statistical uncertainty on the expected number of events. We therefore show results for values of $\alpha$ corresponding to no systematics ($\alpha = 0$) to demonstrate the ultimate precision at the future collider, low systematic uncertainty ($\alpha = 0.05$), and high systematic uncertainty ($\alpha = 0.2$). For the ATLAS analysis of [29] we have deduced that the current systematic uncertainty would correspond to $\alpha \sim 0.063$ and we derive results for an extrapolation to the high-luminosity LHC data set (3000 fb$^{-1}$) either using this value or setting $\alpha = 0$ as the best-case scenario.

We show the resulting constraints on the percent branching ratio in Fig. 4. The values for 95% C.L. upper limits are also given in Table 6. Both the analyses with and without charm-jet tagging are able to provide constraints on the branching ratio of $\mathcal{O}(10^{-3})\%$. A naive statistical combination of the hadronic and semi-leptonic channels yields 95% C.L. upper limits on $\text{BR}(t \to hc)$ of $(8.5 \times 10^{-4})\%$ for the case with charm-jet tagging and $(4.4 \times 10^{-4})\%$ without for the case of no systematics ($\alpha = 0$). For the cases $\alpha = (0.05, 0.2)$ the combination yields: $\text{BR}(t \to hc)$ of $(1.8, 6.1) \times 10^{-3}\%$ for the case with charm-jet tagging and $(2.8, 11.1) \times 10^{-3}\%$ without, respectively. We also show the extrapolation of the ATLAS constraints of [29], which is at least an order of magnitude worse than the results of the present analysis for signal and background.

Table 3 A summary of the selection criteria of the analysis for each of the channels considered for the $pp \to t\bar{t} \to (hc)i$ process. The final invariant mass cut, on $m_{\gamma\gamma}$, allows identification of the signal top quark

| Hadronic: | Semi-leptonic: |
|----------|----------------|
| $\geq 1$ light jets, | $\geq 1$ leptons, |
| top: combine $b$-jet + 1, 2 light jets. | $p_T > 25$ GeV, $|\eta| < 2.5$, |
| $P_{t\to c} = 0.005$, | solve for $P_{t}$ using mass constraint. |
| $P_{b\to c} = 0.125$. | |

$m_{\text{top, reco}} \in [150, 200]$ GeV, $m_{\gamma\gamma} \in [160, 190]$ GeV.

Table 4 The expected signal and background events at an integrated luminosity of $\mathcal{L} = 10$ ab$^{-1}$ after applying the analyses in the search for the $t \to hc$ decay. The resulting event yields are shown for the case where charm-jet tagging is considered for the hadronic and semi-leptonic cases, see main text for further details. As before, the signal cross sections are shown for the working value $\lambda^*_t = 0.1$

| Process | $N_{\text{had}, c\text{-tag}}$ | $N_{\text{had}, c\text{-tag}}$ |
|---------|------------------------------|------------------------------|
| $pp \to t\bar{t} \to (hc)i^+$ h.c. | 22952 | 10260 |
| $pp \to t\bar{t}h$ | 1816 | 689 |
| $pp \to hjjW^\pm$ | 7 | 1 |
| $pp \to \gamma\gamma jjW^\pm$ | 211 | 2 |
| $pp \to t\bar{t}\gamma\gamma$ | 107 | 39 |

Table 5 As for Table 4, but without charm-jet tagging

| Process | $N_{\text{no c-tag}}$ | $N_{\text{no c-tag}}$ |
|---------|----------------------|----------------------|
| $pp \to t\bar{t} \to (hc)i^+$ h.c. | 191871 | 61124 |
| $pp \to t\bar{t}h$ | 26533 | 6962 |
| $pp \to hjjW^\pm$ | 66 | 19 |
| $pp \to \gamma\gamma jjW^\pm$ | 7130 | 164 |
| $pp \to t\bar{t}\gamma\gamma$ | 1598 | 478 |

$\mathcal{L} = 10$ ab$^{-1}$
running at 100 TeV with 10 ab$^{-1}$. We have investigated the rare top quark decay processes.

4 Conclusions

We have investigated the rare top quark decay processes $t \rightarrow bWZ$ and $t \rightarrow hc$ at a future circular hadron collider running at 100 TeV with 10 ab$^{-1}$ of integrated luminosity. We have demonstrated that it will be extremely challenging to observe a final state in which the $t \rightarrow bWZ$ process contributes. This is true even in the case of the presence of new physics contributions allowed by current LHC constraints. On the other hand, the $t \rightarrow hc$ decay can be constrained to $\mathcal{O}(10^{-3})\%$, either with or without considering charm-jet tagging. This estimate is an order of magnitude more stringent than a high-luminosity LHC extrapolation and will allow us to constrain the off-diagonal top quark-charm quark Yukawa couplings to $\lambda_{ct}^h \sim \mathcal{O}(10^{-3})$.

The extremely rare decay modes we have investigated in the present article constitute two of the many interesting ones for top quarks. A future high-energy collider will be able to provide information on other processes, such as $t \rightarrow cWW$, $t \rightarrow q\gamma$, $t \rightarrow qZ$, $t \rightarrow c\gamma\gamma$ and $t \rightarrow cZZ$. We leave investigations of such modes to future work.

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