Self-organized noise resistance of oscillatory neural networks with spike timing-dependent plasticity

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Intuitively one might expect independent noise to be a powerful tool for desynchronizing a population of synchronized neurons. We here show that, intriguingly, for oscillatory neural populations with adaptive synaptic weights governed by spike timing-dependent plasticity (STDP) the opposite is true. We found that the mean synaptic coupling in such systems increases dynamically in response to the increase of the noise intensity, and there is an optimal noise level, where the amount of synaptic coupling gets maximal in a resonance-like manner as found for the stochastic or coherence resonances, although the mechanism in our case is different. This constitutes a noise-induced self-organization of the synaptic connectivity, which effectively counteracts the desynchronizing impact of independent noise over a wide range of the noise intensity. Given the attempts to counteract neural synchrony underlying tinnitus with noisers and maskers, our results may be of clinical relevance.

One of the important features of interacting neurons is the ability to coordinate their firing times and synchronize, which is essentially involved in normal brain function, ranging from sensory information processing to cognitive and motor function. Abnormal neural synchrony, on the other hand, can significantly impair neural processes and is a hallmark of several neurological disorders. Synchronization control became a focus of the research nowadays. It is known that the extent of synchronization in oscillatory networks relates to the amount of coupling among oscillators. An important mechanism that adjusts the synaptic coupling to the underlying neural activity is spike timing-dependent plasticity (STDP), where the synaptic weights are either potentiated or depressed depending on the order of the spike times of pre- and post-synaptic neurons. This mechanism plays an important role in temporal coding of information by spikes.

Synchronized firing of neurons is characterized by narrowly distributed spike times, which, in turn, naturally leads to a potentiation of synaptic weights in neural ensembles with STDP and a stabilization of a strongly coupled and synchronized regime. On the other hand, if synchronization is perturbed, the synaptic weights are depressed until the oscillators get weakly coupled and thus desynchronized. This phenomenon motivated the development of stimulation methods for counteracting pathological neural synchronization. As shown in theoretical studies, animal experiments and in a clinical proof of concept study, desynchronizing stimulation can lead to sustained desynchronization, pronounced normalization of effective connectivity and substantial decrease of symptoms.

Desynchronization can effectively be achieved if the interacting oscillators with fixed coupling are stimulated by independent noise. It is thus to be expected that in neural ensembles with STDP independent noise will cause depression of synaptic weights. Indeed, in order to observe a synaptic potentiation due to STDP, a certain degree of correlation in the input is necessary. We here show that independent noise delivered to the neural population with STDP can surprisingly enhance the amount of synaptic coupling among the neurons, i.e., the neurons counteract the desynchronizing effect of noise by reorganizing their synaptic connectivity and increasing its strength. As a result, the extent of synchronization in a neural ensemble with STDP can be significantly larger as compared to without STDP if both receive an independent noisy input of the same intensity. Put otherwise, STDP leads to self-organized noise resistance. Since noise is inevitable in real systems and, hence, has an impact on neural information processing requiring precise spike timing, our findings show how STDP may be...
involved in a homeostatic mechanism preserving the existing level of collective dynamics in the brain by neutralizing the impact of random perturbations.

**Results**

We first demonstrate the discussed phenomenon for the ensemble of spiking Hodgkin-Huxley (HH) neurons (5)–(7) with STDP and random synaptic input (see Methods). If the input is absent \((I = 0)\), the neurons get strongly coupled, and a uni-directional hierarchical coupling topology is established due to STDP for strong enough initial coupling \([\text{Fig. 1b, SupplementaryFig. S1}]\). If an independent random input is applied to the HH ensemble, the amount of coupling in the perturbed ensemble is significantly enhanced, and, intriguingly, the random perturbations have a constructive effect on the dynamics of the synaptic weights \([\text{Fig. 1a}]\). In fact, the noise promotes the development of bidirectional synaptic connections among neurons \([\text{Fig. 1c}]\), the mean coupling \(K\) increases as the input strength grows, and there exists an optimal noise intensity, where the neurons get maximally coupled \([\text{Fig. 1a}]\). For the considered parameters the optimal input intensity \(I = I_{\text{opt}} \approx 0.14\), where \(K = 0.374\), which corresponds to about 50% of relative increase of the mean coupling with respect to the input-free case. Furthermore, if the noise is not particularly strong, the amount of synchronization in the neural ensemble with STDP is relatively well preserved \([\text{Fig. 1a}]\). For example, for \(I = I_{\text{opt}}\), the time-averaged synchronization order parameter \((R_{\text{STDP}}) \approx 0.82\) for the ensemble with STDP, whereas \((R_{\text{fix}}) \approx 0.21\) for the ensemble without STDP and for fixed coupling matrix \(K_{\text{fix}}\) (see Methods). This corresponds to about 11% and 77% of synchronization suppression relative to the input-free case, respectively. This mechanism constitutes a self-organized resistance to independent noise, where STDP plays a stabilizing role for the synchronized neural firing against the destructive influence of external random perturbations.

The mechanism behind the reported phenomenon is based on the noise-induced dynamics of the spike time differences \(\Delta t_{ij}\) used for the update of the synaptic weights \([\text{Supplementary Section S1B}]\). If the distribution density \(p_i(\Delta t)\) of \(\Delta t_{ij}\) is known, the average update rate of the synaptic weights can be calculated by the integral

\[
\Delta K_{ij} = \int W(\xi) p_i(\xi) d\xi, \quad (1)
\]

where \(W\) describes the update rule in one spike event \((7)\). One therefore has to describe the form of \(p_i\) in order to predict the dynamics of the coupling weights \(k_{ij}\). They will be potentiated if \(\Delta K_{ij} > 0\) and depressed if \(\Delta K_{ij} < 0\). For instance, for a uniform distribution \(p_i = 1/2\sigma\) of \(\Delta t_{ij} \in [-\sigma, \sigma]\), \(\Delta K_{ij} = [k_{1}\tau_1(1 - \exp(-\epsilon/\tau_1)) - A_{2}\tau_2(1 - \exp(-\epsilon/\tau_2))] / 2\sigma\) changes its sign from positive to negative as \(\epsilon\) increases over 5 ms for the considered parameters. Therefore, if \(\Delta t_{ij}\) are broadly distributed, e.g., for desynchronized neurons at a weak initial coupling, the synaptic weights will be depressed and a weakly coupled regime will be realized. On the other hand, a synchronized firing for a strong initial coupling will lead to narrowly distributed \(\Delta t_{ij}\) and further stabilization of a strongly coupled regime \([\text{Fig. 1b}]\), see also Supplementary Section S1A. Notice that the considered STDP will lead to a potentiation of synaptic weights if the neurons fire at a high rate\(^{7,24}\). In this case, the relative spike times will be narrowly distributed even if the neurons are not synchronized. In our case the mean firing rate does not significantly change when the parameters of interest vary \([\text{SupplementaryFig. S3}]\).

We consider the behavior of \(p_i\) in more detail for the phase oscillators \((8)\) with STDP, where we observe the same constructive effect of the independent noise: As the noise intensity increases, so does the mean coupling strength \(K\) until it reaches its maximal value at the optimal noise intensity \(\mu = \mu_{\text{opt}}\) \([\text{Fig. 2a}]\). As for the HH ensemble, the noise induces the emergence of bidirectional coupleings among oscillators \([\text{Fig. 2b}]\), and STDP counteracts the suppression of synchronization by the noise \([\text{Fig. 2a}]\). Although the latter effect for the phase ensemble is somewhat less pronounced \((\text{regarding} \langle R_{\text{STDP}} \rangle / \langle R_{\text{fix}} \rangle)\) than for the HH neurons, we still observe the self-organized resistance to noise for the phase oscillators mediated by STDP, where \(\langle R_{\text{STDP}} \rangle > \langle R_{\text{fix}} \rangle\).

We found that the emergence of positive couplings below the diagonal in the coupling matrix \([\text{Fig. 2b}]\) of the phase ensemble can be explained by evaluating the impact of the noise on the phase differences for fixed coupling matrix \(K_{\text{fix}}\), and we consider such a system below.

In the strongly coupled regime without noise the oscillators are phase locked and the phase differences are constant. The following recurrent formula gives the constant phase shifts of the locked phases \(\psi_i = \omega t + \phi_i\) (see Supplementary Section S2A):

\[
\phi_i = \arcsin \left( \frac{S_i + 1}{\sqrt{D_i + 1}} \right) + \arcsin \left( \frac{N \bar{\omega}_i}{k \sqrt{D_i + 1}} \right), \quad (2)
\]

where \(D_i + 1 = S_i + C_i^2, S_i + 1 = \sum_{j=1}^{N} \sin(\delta_j), C_i + 1 = \sum_{j=1}^{N} \cos(\delta_j)\), and \(\bar{\omega}_i = \omega_i - \omega_N\). Letting \(\omega_N = 0\), without loss of generality, we find the constant phase differences \(\Delta \psi_i = \phi_i - \phi_N\) for weak to moderate noise the phase differences fluctuate around the above mean values and get broadly distributed, see Fig. 3a, Supplementary Section S2B, and Refs. 25, 26. Since the phase differences obey a circular statistics we approximate them in the noisy case by the von Mises distribution\(^{27}\).
therefore represent the dependence of parameter \( k \) and ratio \( \langle R_{\text{STD}} \rangle / \langle R_{\text{fix}} \rangle \) (scale on the right vertical axis) between the time-averaged order parameters for the ensemble with and without STDP, respectively, versus noise strength \( \mu \). In the latter case the coupling matrix is fixed \( K_{\text{fix}} \) (see Methods). (b), Coupling matrix \( K_{\text{STD}} \) established in the phase ensemble due to STDP for the noise intensity \( \mu = 0.1 \). The dashed black curve in (a) approximates the mean coupling weight \( K \), and the white curve in (b) bounds the region of potentiated coupling weights, both as predicted by the theory (see text for details). The oscillators are sorted with respect to increasing natural frequencies \( \omega_i \), which are uniformly and randomly distributed in the interval \([0.9, 1.1] \).

\[
M(\kappa, \varphi) = \frac{1}{2 \pi I_0(\kappa)} \exp(\kappa \cos(\varphi - \varphi_0)),
\]

where \( I_0(\kappa) \) is the modified Bessel function of first kind and zero order, \( \kappa \) is the concentration parameter, and \( \varphi_0 \) is the mean value. The parameter \( \kappa(\Delta \psi_{ij}) \) can be determined and demonstrates a power-law dependence on the noise strength \( \mu \) [Fig. 3b]

\[
\kappa(\Delta \psi_{ij}) = F(\omega_i, \omega_j) \mu^\gamma, \quad F(\omega_i, \omega_j) = \beta \frac{\omega_i \omega_j}{\omega_i + \omega_j},
\]

where the exponent \( \gamma = -2 \) seems to be independent of the natural frequencies \( \omega_i \) and \( \omega_j \) [Fig. 3b and Supplementary Section S2B]. We therefore represent the dependence of parameter \( \kappa(\Delta \psi_{ij}) \) on the natural frequencies as a function \( F(\omega_i, \omega_j) \) in equation (4). Detailed numerical calculations reveal that the contour lines \( F(\omega_i, \omega_j) = F_{\text{const}} \) of the function \( F \) align along the hyperbolas \( \beta \omega_i \omega_j = F_{\text{const}} (\omega_i + \omega_j) = 0 \) for some constant \( \beta \), where \( \beta = 9.52 \) for the considered fixed other parameters of the system, see Supplementary Section S2C.

With the use of equation (4) one can predict the noise-induced emergence of positive coupling \( k_{ij} \) from slow oscillators to fast ones, (for indices \( j < i \) in Fig. 2b). For this, the STDP function (7) can be integrated with respect to the distribution density \( \rho(\Delta \psi_{ij}) \) of the form (3) according to equation (1) for the mean phase differences (2) and parameter \( \kappa \) from equation (4) with the obtained parameters \( \gamma \) and \( \beta \). The results of such an approximation are illustrated in Figs. 3c, d, where the range of potentiated coupling weights increases as predicted by \( \Delta k_{ij} > 0 \) [Fig. 3c] which is in good accordance with the numerical simulations for weak to moderate noise [Fig. 3d]. Moreover, the above equations can effectively be used to approximate the mean coupling [Fig. 2a] and the shape of the coupling matrix with irregular border between potentiated and depressed coupling weights [Fig. 2b] for randomly distributed natural frequencies.

Strong noise destroys the synchronization in the HH and phase ensembles, which, in turn, leads to a depression of the coupling among oscillators by STDP, and the mean coupling weight \( K \) nearly vanishes [Figs. 1a and 2a]. We found that the onset of decoupling
originates from the fast oscillators (large index \( j \) in Figs. 1c and 2b) and propagates to the interior of the coupling matrix as time evolves, see Supplementary Videos 1 and 2 for the animated time courses of the coupling matrices of the HH and phase ensembles, respectively. The indication of such a decoupling mechanism can be obtained from the population without STDP and fixed coupling matrix \( K_{\text{fix}} \) (see Methods). Already for \( \mu = \mu_{\text{opt}} = 0.1625 \) the coupling weights \( k_{ij} \) from the fastest oscillators are predicted to be depressed by STDP as, for example, for \( i = 100 \) and \( j = 200 \), where \( \Delta k_{100,200} < 0 \) [Fig. 3c]. This indicates that the suppression of the coupling for large noise will start from the fastest oscillators.

For the same parameters of the STDP function (7) the self-organized resistance against noise is significantly enhanced for another, multiplicative (state-dependent) update rule, where the coupling weights are changed relative to their current values \( k_{ij} \rightarrow k_{ij} + (k_M - k_{ij})\delta W(\Delta \psi_{ij}) \), where \( k_M = k_{\text{max}} \) or \( k_M = k_{\text{min}} \) depending on whether the coupling update \( \delta W(\Delta \psi_{ij}) \) is positive (potentiation) or negative (depression), respectively\(^{28}\). Even for strong independent noise the oscillators with such a coupling update remain strongly coupled and synchronized [Fig. 4a]. The dynamics of the coupling matrix is, however, different for this update rule [Fig. 4b]. As the noise strength increases, the coupling weights \( k_{ij} \) converge from a strictly bimodal distribution for the noise-free case via a nearly uniform distribution to a well-pronounced uni-modal distribution of approximately globally coupled oscillators for strong noise. The latter distribution is in accordance with the results of Ref. 28. Interestingly, the oscillators are coupled with about the same mean coupling in the noise-free case (\( \mu = 0 \)) and for strong noise (\( \mu = 0.5 \)) [Fig. 4a]. In the latter case, however, the population with STDP is much more resistant to noise than the population without STDP, while both have the same mean coupling. This also indicates that the global coupling with narrowly distributed coupling weights [Fig. 4b] is more favorable if robustness of the synchronized dynamics against noise is required. These findings also contribute to the problem of the optimal coupling topology for easily synchronizable networks and their resistance to noise\(^{29}\).

**Discussion**

We demonstrated the constructive impact of independent noise on ensembles of oscillatory HH neurons and phase oscillators with asymmetric STDP and for two different protocols of the coupling update based on the difference of either the spike timing or the phases. In the latter case the coupling update is separated from possible changes of the frequencies, which means that the reported phenomenon is in fact based on the phase dynamics. This mechanism is different as compared to stochastic or coherence resonances\(^{30–32}\), where the interplay between noise-induced and internal or external times scales is important. Indeed, the noisy input does not significantly change the frequency of the synchronized neurons and only influences the distribution of the phase differences by broadening it [Fig. 3c]. This results in a potentiation of the synaptic weights that were depressed in the noise-free case.

For the phase model we provided a theoretical approximation of the structure of the coupling matrix, which is in good agreement with the results of the numerical simulations. For the HH ensemble we also verified the reported phenomenon for a random synaptic inhibitory input and somatic Gaussian noise as well as for different spike pairing for STDP [Supplementary Section S1C]. Furthermore, we verified the phenomenon for different parameter sets for the plasticity function and found that the noise-induced increase of synaptic weights gets more pronounced if the STDP function is shaped for a stronger potentiation rather than for depression. In this study we however considered a non-trivial case, where strongly coupled synchronized and weakly coupled desynchronized states stably coexist if the communication delay among neurons is small, and synchronization is associated with large coupling\(^{33,34}\). In general, the noise-induced increase of the mean coupling can be expected for an asymmetric STDP rule if the neurons can be in-phase locked with narrowly distributed spike time differences, and a uni-directional coupling topology like in Fig. 1b is established in the noise-free case.

The resonance-like behavior of the mean coupling versus noise intensity has been observed for both multiplicative and additive coupling update rules, where the coupling update either depends or not, respectively, on the current value of the synaptic weight and leads to “soft” or “hard” bounds, accordingly\(^{15,28}\). The distribution of synaptic weights however is always bimodal for hard bounds [Figs. 1 and 2], whereas it undergoes a gradual transformation from a bimodal to a uniform distribution and then to a relatively narrow unimodal distribution as noise strength increases for soft bounds [Fig. 4], see also Refs. 23, 28. These findings point to the robustness and generality of the reported phenomenon.

Our results suggest a possible homeostatic mechanism of how the brain may counteract external perturbations and noise in order to preserve the existing level of neural synchrony and bridge the transition from information coding by precise spike times to variable and imperfect spike timing. Noise leads to the development of bidirectional coupling among neurons observed in experiments\(^{35}\). Furthermore, our results show that independent noise can by no means be considered as an effective method for desynchronization of oscillatory neural networks with STDP. Also from the clinical standpoint our results may be important. In fact, they may contribute to a deeper understanding of why maskers and noisers show limited efficacy in counteracting tinnitus\(^{36}\), the latter being associated with abnormal neural synchrony\(^{4,20}\).

**Methods**

Hodgkin-huxley (HH) ensemble. The considered system of \( N \) synaptically interacting spiking HH neurons\(^{37,38}\) reads

![Figure 4](https://www.nature.com/scientificreports)
where the coupling weights \(k_{ij}\) obey the STDP rule (7) with parameters \(A_1 = 1, A_2 = 0.5, \tau_1 = 0.45, \tau_2 = 1.5, \text{ and } \delta = 0.005\), and are confined to the interval \(k_{ij} \in [k_{\text{min}} \text{ to } k_{\text{max}}] \) with \(k_{\text{min}} = 0 \text{ and } k_{\text{max}} = 1\). The update (7) of the coupling coefficients is based on the phase difference \(W = (\psi_j(t) - \psi_i(t))\), \(\psi_j(t) - \psi_i(t)\) between the pre- and postsynaptic oscillators \(j \text{ and } i\), respectively, and undertaken when their phases cross zero (mod 2\(\pi\)), which is declared as a spike onset if the phase visited an “inter-spike” value \(\pi \text{ (mod } 2\pi)\) just before. The phase-based STDP was chosen in order to avoid any influence of the frequency dynamics and to show that the discussed effects are based on the phase-induced dynamics of the phase differences. The phase oscillators (8) are perturbed by a normally distributed independent noise \(\zeta_i(t)\) and \(\zeta_j(t)\), and \(\eta_i(t)\) and \(\eta_j(t)\), and \(\eta_j(t)\), respectively, and intensity \(\eta_i(t)\) and \(\eta_j(t)\) are uniformly and randomly distributed in the interval \([0.9, 1.1]\). In calculations for fitting the noise-induced distribution of the phase differences we also used a regular distribution \(\eta_i(t)\) and \(\eta_j(t)\) of \(0.9 \pm 0.2(t - t_1)/N(1-1)\). For numerical integration of model (8) with noise input we used the Heun method with step size 0.01.

As for the HH neural ensemble, the noise-free \((\mu = 0)\) phase ensemble (8) with the phase-based STDP (7) demonstrates a multistability of a weakly coupled asynchronous regime (with \(K = 0.11\) and \(R = 0.4\)) and a strongly coupled synchronized regime (with \(K = 0.5\) and \(R = 0.98\)). In the latter regime a unidirectional hierarchical coupling from fast to slow oscillators is established, similarly to the HH neural population, see Fig. 1b.

**Fixed coupling.** To compare the effect of the noise for the HH and phase ensembles with STDP to those without STDP, in the latter case the coupling matrix was fixed to \(K_{\text{fix}}(i,j)\) where \(k_{ij} = k = k_{\text{max}} = 2 \text{ for } i < j\) and \(k_{ij} = 0\) otherwise (the oscillators are sorted with respect to increasing natural frequency), as for the strongly coupled regimes established without noise.

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**Additional information**

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