Origin and evolution of two-component debris discs and an application to the $q^1$ Eridani system

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ABSTRACT
Many debris discs reveal a two-component structure, with an outer Kuiper-belt analogue and a warm inner component whose origin is still a matter of debate. One possibility is that warm emission stems from an “asteroid belt” closer in to the star. We consider a scenario in which a set of giant planets is formed in an initially extended planetesimal disc. These planets carve a broad gap around their orbits, splitting up the disc into the outer and the inner belts. After the gas dispersal, both belts undergo collisional evolution in a steady-state regime. This scenario is explored with detailed collisional simulations involving realistic physics to describe a long-term collisional depletion of the two-component disc. We find that the inner disc may be able to retain larger amounts of material at older ages than thought before on the basis of simplified analytic models. We show that the proposed scenario is consistent with a suite of thermal emission and scattered light observational data for a bright two-temperature debris disc around a nearby solar-type star $q^1$ Eridani. This implies a Solar System-like architecture of the system, with an outer massive “Kuiper belt”, an inner “asteroid belt”, and a few Neptune- to Jupiter-mass planets in between.

Key words: circumstellar matter – stars: individual: $q^1$ Eri (HD 10647, HIP 7978) – infrared: planetary systems – submillimetre: planetary systems – methods: numerical

1 INTRODUCTION
Debris discs, dusty belts of planetesimals around stars, are natural by-products of planet formation. While far-infrared observations of the past decades typically revealed cold, distant dust stemming from Kuiper belt analogues, recent observations and analyses demonstrate that many discs possess a rich radial structure. There are systems such as Fomalhaut and Vega where dust appears to be present all the way through from more than a hundred au to the sublimation zone at a few stellar radii (e.g., Su et al. 2013; Lebreton et al. 2013).

The presence of material in the cavities of the main, cold discs seems to be a rule rather than an exception. Indeed, about two-thirds of debris disc systems around late-type stars may exhibit an additional warm component (e.g., Morales et al. 2011; Ballering et al. 2013; Chen et al. 2014; Pawellek et al. 2014; Kennedy & Wyatt 2014). The nature of that warm component remains a matter of debate. One possibility is to attribute the warm dust emission to an inner planetesimal belt, i.e. to an asteroid belt analogue. By analogy with the Solar System with its Kuiper belt and asteroid belt, such a two-component structure could be created by a set of giant planets. If these succeeded to form in the disc, they would carve a hole in the protoplanetary disc by removing neighbouring dust and gas (Dipierro et al. 2016, and references therein). After the gas dispersal, nascent planets would swiftly remove planetesimals from their chaotic zones. At the same time, these planets would dynamically excite planetesimals in the zones bracketing the planetary region, preventing their further growth to full-size planets. All this would generate a broad gap in the planetary region, splitting up the disc into two distinct debris belts. So far, the presumed inner belt may have been marginally resolved for two systems, $\varepsilon$ Eri (Greaves et al. 2014) and HD 107146 (Ricci et al. 2015a).

Instead of being locally produced in an “asteroid belt”, warm dust can be transported inward from outer production zones by Poynting-Robertson and stellar wind drag. For low-density systems where collisional timescales are longer than the one for transport, the inner disc region is filled by dust, leading to a nearly uniform density profile (Wyatt 2005; Kennedy & Piette 2015). This scenario is able to explain the observed emission of discs around late-
type stars such as \( \epsilon \) Eri (K2 V), HIP 17439 (K2 V), and AU Mic (M1 V) as shown previously by means of collisional modelling (Reidemeister et al. 2011; Schüppler et al. 2014, 2015). However, this may not be a viable alternative for discs around earlier-type stars where no strong stellar winds are expected.

In this paper, we consider the debris disc around the nearby F-star \( q^1 \) Eridani. Among the discs observed with Spitzer and Herschel, the \( q^1 \) Eri system is outstanding for having a strong infrared excess with a fractional luminosity (infrared luminosity of the disc divided by the stellar luminosity) of about \( (2 \pm 3) \times 10^{-4} \) (Trilling et al. 2008; Eiroa et al. 2013). The disc has been spatially resolved in the far infrared (Liseau et al. 2008, 2010) and in the scattered light (K. Stapelfeldt, priv. comm.). The images reveal a bright disc with a radius of \( \sim 100 \) au. The mid-infrared Spitzer/IRS spectrum between 20 and 30 \( \mu \)m (Chen et al. 2006) clearly hints at the presence of an additional warm debris component, which is unresolved in the images. The fractional luminosity of the warm component is \( \sim 10^{-5} \), which is only a factor of several lower than that of the main disc. Attempts to reproduce the data with a two-component model require the warm dust to be located at several au from the star (Tanner et al. 2009; Pawellek et al. 2014). Apart from the two-component disc, a Jupiter-mass planet with a semi-major axis of 2 au and an eccentricity of 0.15 has been detected by radial velocity measurements (Butler et al. 2006; Marmier et al. 2013). The region inside the planetary orbit seems to be largely free of dust as there is no detection of near-infrared excess, associated with the presence of hot exozodiacal dust (Ertel et al. 2014).

Explaining the architecture of the \( q^1 \) Eri disc is a challenge. Since \( q^1 \) Eri is an F star, we do not expect strong stellar winds, and the Poynting-Robertson drag alone would be inefficient in delivering an amount of material sufficient to explain the warm dust emission. This might reinforce the planetary scenario described above, in which the system would be reminiscent of the Solar System’s two-belt architecture with a set of invisible planets between the belts. However, this explanation is questionable, too. It is well known that the fractional luminosity of a debris belt collisionally evolving in a steady-state regime cannot exceed a certain value for a given system’s age (Wyatt et al. 2007; Löhne et al. 2008). That limit is more stringent for older systems and for belts closer to the star where the collisional decay is faster. Assuming plausible parameters, the model by Wyatt et al. (2007) suggests that the warm dust in the \( q^1 \) Eri disc may be indeed too bright, and the system too old, to be compatible with a steady-state collisional cascade in an “asteroid belt”. If true, this would probably leave us with a possibility that the observed warm dust is an aftermath of a recent major collision between two big planetesimals. However, this comes with the caveat that such events in gigayear-old systems may not be likely either.

In this paper, we show that the Solar System-like planetary scenario may work, contrary to what simplified models of the long-term collisional decay may suggest. We present a model to explain the formation of both components of the \( q^1 \) Eri disc self-consistently. To this end, we simulate the collisional evolution of an initially extended planetesimal distribution, assumed to be typical for the end stage of a protoplanetary disc, and let it evolve over the age of the \( q^1 \) Eri system. Our simulations predict the radial and size distribution of the produced dust as a function of time, from which thermal emission properties are calculated to compare with observations. The goal is to see whether a sufficient amount of material can survive in the inner region of the system against collisional depletion to reproduce the available observational data.

Section 2 presents the long-term collisional evolution of fiducial debris discs. In Sect. 3, we give an overview of the thermal emission data, obtained for the \( q^1 \) Eri system, and apply the collisional modelling to the \( q^1 \) Eri disc. Section 4 contains a discussion and Sect. 5 lists our conclusions.

2 LONG-TERM COLLISIONAL EVOLUTION MODEL

2.1 Modelling method

We perform the modelling with the ACE code (Krivov et al. 2006; Löhne et al. 2012; Krivov et al. 2013), which simulates the collisional evolution of debris discs. Starting from an assumed initial distribution of planetesimals, the code calculates the production and loss of material in a collisional cascade by solving the Smoluchowski-Boltzmann kinetic equation. Radiative and corpuscular forces acting on the disc particles are also included. ACE provides coupled spatial and size distributions of the objects within the disc, ranging from \( \sim 100 \) km-sized planetesimals down to submicron-sized dust grains.

The code uses object masses, pericentric distances, and eccentricities as phase-space variables and assumes the disc to be rotationally symmetric. Particle densities are averaged over the inclination, from zero to the disc’s semi-opening angle, which is fixed to half the maximum eccentricity of the planetesimals. The outcome of a two-particle collision is controlled by the specific energy threshold for disruption and dispersal. We use the specific disruption energy, \( Q_{\text{bd}} \), as expressed in equation (7) of Löhne et al. (2012), which is a sum of two power laws for the particle size ranges where \( Q_{\text{bd}} \) is dominated by tensile strength and self-gravity. Following the values of basalt presented in Benz & Asphaug (1999), we assume \( Q_{\text{bd}} = Q_{\text{bd}, \text{g}} = 5 \times 10^6 \) erg g\(^{-1} \), \( b_1 = -0.37 \), and \( b_2 = 1.38 \). If the specific impact energy of a collision exceeds the threshold \( Q_{\text{bd}} \), the target breaks apart and the collision is treated as disruptive. Beside disruptive collisions, the code also considers cratering, where the target is cratered only while the projectile is disrupted, and bouncing collisions, where the target stays intact and the projectile is cratered. The mass distribution of fragments for each collision is assumed to follow \( n \sim 1.83 \), which is the equilibrium value averaged over many collisions (Thébault & Augereau 2007). Dust transport within the \( q^1 \) Eri disc is assumed to play a minor role. Hence, we do not take Poynting-Robertson and stellar wind drag into account in the simulations presented in this paper.

2.2 Extended planetesimal disc

We first consider the long-term collisional evolution of an initially extended planetesimal disc, which is a likely remnant of the planetesimal formation process. In this section, we seek to understand the general features of collisional evolution predicted by our simulations. Therefore, we generated a representative setup by using a set of standard assumptions that are not yet adjusted to the \( q^1 \) Eri system.

We assumed a planetesimal distribution between 1 and 100 au around a solar-type star, having a solid surface density of the standard Minimum Mass Solar Nebula (MMSN) model: \( \Sigma = 1 M_\oplus \text{ au}^{-2} (r/\text{au})^{-1.5} \) (Weidenschilling 1977; Hayashi 1981). The disc was filled with planetesimals up to 100 km in radius. We set the orbital eccentricities of the planetesimals to a mean value of 0.05, in agreement with values expected for discs around solar-type stars (e.g., Pawellek & Krivov 2015). Also, smaller bodies were already present within the disc at the beginning of the simulation.
The initial size distribution of the bodies followed $s^{-3.7}$, which is the equilibrium distribution of dust in an infinite collisional cascade for the material parameters in the strength regime given in Sect. 2.1 (O’Brien & Greenberg 2003). This particular choice does not really matter, since the simulation promptly drives the system to an equilibrium size distribution that does not depend much on the one assumed initially. This comes with the caveat that the kilometre-sized and larger planetesimals in the outer disc do not reach a collisional equilibrium by the end of the simulation and may retain their primordial distribution set by their formation process (which is poorly known anyway). The smallest particles considered in the simulation had radii of $\approx 0.5 \mu m$ that corresponds to the blowout radius, $s_{\text{blow}}$, of silicate grains around a solar-type star. Grains smaller than $s_{\text{blow}}$ were neglected because they are pushed on unbound orbits through the direct radiation pressure and are expelled from the system on dynamical timescales.

Top panels in Fig. 1 depict the evolution of the mass surface density, $\Sigma$, and the normal optical depth, $\tau_\perp$, as functions of distance from the star. While $\Sigma$ reflects the distribution of kilometre-sized, massive bodies, $\tau_\perp$ traces the distribution of micron-sized dust grains that dominate the cross section. This difference is best illustrated by considering the region beyond 100 au. In this zone, the disc mass surface density is negligible, while the optical depth shows a halo that contains small grains with radii slightly above $s_{\text{blow}}$. These grains are in eccentric orbits with pericentres within the planetesimal zone and apocentres outside.

Bottom panels in Fig. 1 depict the size distributions close to the inner (4 au) and outer (94 au) edge of the planetesimal disc. The size distributions exhibit a wavy pattern which is more pronounced towards the dust size range (radii $<1 \mu m$), since there are no grains below $s_{\text{blow}}$ that could work as destructive projectiles (Campo Bagatin et al. 1994; Krivov et al. 2006; Thébault & Augereau 2007; Wyatt et al. 2011).

Both the radial profiles and the size distributions change with time. This evolution is described and discussed in detail below, and we start with the initial stage. The top right panel of Figure 1 reveals an extremely high initial optical depth ($> 10$ at 1 au), in the innermost regions of the disc. It arises because ACE takes the initial slope of the $\Sigma$ profile and populates the disc initially by small, micron-sized grains in accord with the $s^{-3.7}$ power law. However, as explained above, that power law tacitly assumes that the system has an equilibrium distribution of an idealised, infinite collisional cascade from the very beginning. Obviously, this assumption is not valid for a debris disc right after its birth. Instead, the initial distribution of dust in a young debris disc must be the one set by physical processes that operated in the preceding protoplanetary disc by the time of the gas dispersal. On any account, ACE gets rid of the “unphysically” overabundant dust particles swiftly and the optical
depth drops to the equilibrium values after a few thousand years. Already at 1 Myr, the $\tau_\perp$ curve in Fig. 1 is flat, regardless of the profile assumed initially.

The subsequent evolution of the disc depends on the collisional lifetimes of the disc particles and can be understood as follows. Since collisional lifetimes get longer with increasing particle size and distance from the star, modifications of the size distributions go from small to large objects and from inner to outer disc regions. The small dust that dominates the optical depth depletes and reaches collisional equilibrium first, larger objects follow. As a result, at times shorter than the collisional lifetime of the largest objects at a given distance, $\tau_\perp$ decreases faster than $\Sigma$ does. It is this gradual inside-out, bottom-up transition of the size distribution from the initial to the quasi-equilibrium state combined with the initial radial distribution that explains why the radial profiles of $\tau_\perp$ are almost flat, even though the $\Sigma$ profiles are not.

Once the lifetimes of the biggest objects are reached at a given distance, the local size distribution keeps its shape, while $\Sigma$ and $\tau_\perp$ both deplete with their mutual ratio staying constant. After tens of megayears, material is sufficiently eroded to generate positive slopes of both $\Sigma$ and $\tau_\perp$ in the inner regions.

After 1 Gyr, almost all material is reprocessed and only the largest planetesimals in the outer disc have not yet started to deplete collisionally and follow their primordial size distribution. This is seen for objects larger than 10 km at 94 au.

For the sake of comparison, the analytic steady-state evolution model of Wyatt et al. (2007) is overplotted in Fig. 1. Their model was designed to describe the evolution of a narrow debris disc, but can readily be applied to an extended debris disc, assuming it to consist of non-interacting concentric annuli (Kennedy & Wyatt 2010). To enable direct comparison, we converted the maximum disc mass $M_{\text{max}}$ and the maximum fractional luminosity of the dust $f_{\text{max}}$ of Wyatt et al. (2007) to the surface density and the normal optical depth:

$$\Sigma(r, t) = \frac{M_{\text{max}}}{2\pi r^2 \Delta \Sigma},$$

$$\tau_\perp(r, t) = \frac{\sqrt{2}}{\Delta \Sigma} f_{\text{max}}(r, t),$$

where $r$ is the radius and $\Delta \Sigma$ the width of a planetesimal ring. We also calculated the evolution of the size distributions by means of the equations (1), (13), and (14) of Wyatt et al. (2007).

The parameters of the Wyatt et al. (2007) model were chosen in such a way that it matches the ACE run as closely as possible. Accordingly, all parameters that are shared by the analytic model and the ACE simulation were set to the same values. These include the stellar mass and luminosity, the initial disc mass, the eccentricity of the planetesimal orbits, and the diameter $D_\text{f}$ of the largest planetesimals in the collisional cascade.

There are two important parameters, however, for which the best choice is less obvious. One is the slope $(2 - 3q)$ of the size distribution, which is not an input parameter of the ACE simulation. We assumed $q = 11/6$, or $2 - 3q = -7/2$. Another parameter is the specific disruption energy $Q_\ast$, which must be independent of size in the Wyatt et al. (2007) model. We chose $Q_\ast = 10,000$ J/kg, which is representative for two different particle populations. Indeed, since $Q_\ast$ used in ACE has a V-like shape in a log-log scale with a minimum at around 100 m, any constant value above this minimum intersects the two branches in the small and large particle size range. The assumed $10,000$ J/kg corresponds to the material strength of planetesimals with a few tens of kilometres in radius as well as of millimetre-sized grains. The latter are important sources for the production of yet smaller dust that mainly determines the optical depth. Thus, our choice of $Q_\ast$ ensures that particles from the lower and upper end of the wide size range are taken into account.

As can be seen in Fig. 1, the ACE simulation predicts a significantly higher mass surface density at later times than the analytic model of Wyatt et al. (2007). This is a consequence of a slower depletion of the planetesimals best visible in the size distributions at 4 au. In contrast to the analytic reference, the ACE simulation involves a size-dependent $Q_\ast$. The lifetimes of the largest planetesimals are longer, because their $Q_\ast$'s exceed the value of 10,000 J/kg adopted in the analytic model by a factor of several. Furthermore, the $Q_\ast$'s of the planetesimals increase with object size as a result of self-gravity. The latter effect enhances the abundance of larger planetesimals relative to their disruptive projectiles. The slope of the resulting steady-state size distribution of the largest planetesimals flattens with respect to that in the strength regime or the canonical $r^{-3.5}$ (O'Brien & Greenberg 2003). Thus, at later times, the ACE simulation retains a reservoir of large planetesimals that is more massive and is able to sustain a given optical depth or dust mass for a longer period of time than the analytic model.

### 2.3 Two narrow planetesimal discs

We now consider the evolution of a disc whose radial structure was additionally sculpted by the formation of planets. The primary effect of giant planet formation, which we only consider here, is the opening of a planetary gap that splits up the disc. Since such a gap is already produced before the debris disc phase, we can take it into account through a suitable choice of the initial density profile.

Accordingly, we cut out two regions of the extended planetesimal disc presented in the previous section. The inner disc was assumed to lie between 3 and 10 au, the outer disc between 70 and 100 au. Other initial parameters were the same as explained for the extended disc. In particular, the initial surface density of both belts followed the MMSN description. The two belts were then evolved with two independent ACE runs.

Figure 2 compares the two-component system with the extended disc. At any given age, the surface densities in the two models are very close (Fig. 2, top left). There are, however, some deviations between the shape of the size distributions in the two models, especially in the outer zone (Fig. 2, bottom right). These deviations are related to the collisional interaction of different disc regions. In the extended disc model, the dust grains with sizes just above the blowout size, produced at a certain distance, are sent by radiation pressure to eccentric orbits, and therefore, enter the outer disc zones where they collide with the local material. This causes an overabundance of grains just above the blowout limit, which enhances the depletion of larger grains. This effect favours the formation of distinct dips in the size distributions, as seen around 5 $\mu$m at 94 au. Since the two-component model simulates the two belts independently, such a collisional interaction is neglected, and so, the dips are absent. As a consequence, the planetesimal rings of the two-component model tend to have somewhat higher optical depths than in the extended disc simulation (Fig. 2, top right).

We emphasize that our model treats the evolution of the inner and outer planetesimal belts self-consistently since both originate from a common initial surface density profile. Possible interactions with one or more planets within the gap that separates the two components are not directly included. However, such interactions can be taken into account through the choice of initial disc parameters. For instance, the gap width reflects the number and mass of planets.
3 APPLICATION TO q1 ERI

3.1 Star

We took stellar parameters from the Herschel/DUNES final archive (Eiroa et al. 2013). The star has the spectral type F8 V, a luminosity of 1.5 \( L_\odot \), an effective temperature of 6155 K, a mass of 1.12 \( M_\odot \), a metallicity of \([\text{Fe/H}] = -0.04\), and a surface gravity of log(\( g \)) = 4.48 (CGS). The star is at a distance of 17.4 pc (van Leeuwen 2007).

We adopted the stellar photosphere model from Eiroa et al. (2013), which has been obtained by an interpolation in the PHOENIX/GAIA model grid (Brott & Hauschildt 2005) with a normalisation to optical and WISE fluxes.

Age estimations of q1 Eri span a wide range, from 0.3 to 4.8 Gyr (Liseau et al. 2008, and references therein). However, the strength of chromospheric activity and the luminosity in X-rays suggest that the star is \( \gtrsim 1 \) Gyr old. In this paper, we assume an age of around 1 Gyr.

3.2 Observational data

Photometric data have been collected from the Herschel/DUNES archive\(^1\) and the literature. From the set of available data, we use the measurements that are at least 1 \( \sigma \) above the stellar photosphere model, thus indicating the infrared excess (Table 1). A Spitzer/IRS spectrum, reduced by the c2d Legacy Team Pipeline, was also taken from the DUNES archive.

In addition, we extracted radial surface brightness profiles from the Herschel/PACS images provided in the DUNES archive. At 70, 100, and 160 \( \mu m \), cuts were performed along the minor and major axes of the observed disc, with position angles of 144° and 54° east of north, respectively. The stellar position was assumed to coincide with the intensity-weighted centroid of the disc. Profiles of the minor and major axes were obtained by averaging the two sides of the disc. Uncertainties in intensity are dominated by differences between opposing branches of both axes, added in quadrature to a minor contribution from background noise that was estimated from an annular aperture. The resulting profiles and error bars are depicted in Fig. 3. Horizontal error bars reflect the bin widths in the underlying images: 1” at 70 and 100 \( \mu m \), 2” at 160 \( \mu m \).

3.3 Two-component model

As explained in Sect. 1, the q1 Eri system shows strong indications for harbouring a two-component debris disc. We performed additional tests to confirm that the presence of a warm component is certain. One test was to vary the effective temperature of the star by \( \pm 100 \) K, which is the scatter in the literature values (Nordström et al. 2004; Chen et al. 2006). For each stellar temperature, we generated a photospheric model and then fitted two-component disc models to the SED, assuming the dust distribu-

\(^1\) http://sdc.cab.inta-csic.es/dunes/jsp/homepage.jsp
tions to follow power laws. The warm components inferred were moderately different. However, in all the cases a warm component was clearly needed to explain the data. Another test was to overplot the q$^1$ Eri system in figure 5 of Kennedy & Wyatt (2014) that presents a $\chi^2$ map calculated from fitting a single-temperature blackbody (i.e., a one-component disc) to fiducial two-temperature (i.e., two-component) discs. We find q$^1$ Eri to lie close to the contour line $\chi^2_{\text{red}} \approx 20$, meaning that this system is highly inconsistent with a one-component structure. Finally, we estimated an uncertainty in the normalisation of the photospheric model to the optical fluxes to be about 2%. A two-component fitting similar to that described above, but with the photospheric model made by 2% brighter, also showed that the warm component was needed to reproduce the SED.

Given these results, we applied the ACE-based two-component model presented in Sect. 2.3 to explain the SED and the Herschel surface brightness profiles of the q$^1$ Eri system. We assumed the stellar properties as described in Sect. 3.1 and simulated a set of several two-component models where we varied the following parameters: the location, width, and initial mass (in terms of the MMSN multiples) of the inner and outer components, the eccentricities of the planetesimal orbits, the size of the largest planetesimals, and the chemical composition of the disc particles. For the purpose of surface profile modelling, we generated synthetic images from the ACE models at 70, 100, and 160 $\mu$m with a position angle of 54.2° (east of north), which is the mean value seen in the three Herschel/PACS images. The synthetic images were then convolved with a Boo PSF. The PSFs were rotated by 83° counter clockwise to align the maps with the telescope pupil orientation on the sky during the q$^1$ Eri observations.

Fitting the model to the observational data is challenging, because we can only vary the parameters of the parent planetesimals and not the dust distributions. The impact of parameter variations on the resulting dust distributions, and thus, on the thermal emission properties is difficult to predict quantitatively. Several time-consuming trial-and-error ACE simulations are necessary to change the dust distribution in a desired way. Furthermore, different combinations of disc parameters can produce similar SEDs and brightness profiles, and therefore, a unique solution does not exist. We aimed at finding one plausible model that agrees with the observations reasonably well. We probed various maximum orbital eccentricities of planetesimals (0.03, 0.05, and 0.1) and their largest radii (50 and 100 km). Inner and outer edges of the inner planetesimal belt were varied between 3 and 20 au, and those of the outer belt between 65 and 135 au. We assumed dust particles to be a mixture of astrosilicate (Draine 2003) and water ice (Li & Greenberg 1998) and chose the volume fraction of ice to be a free parameter. Ice fractions of 0, 50, 70, and 90 per cent were explored.

We finally achieved the model presented in Fig. 3. The corresponding parameters are summarised in Table 2. The model profiles overpredict the 160 $\mu$m emission in the central region by $\approx 20$ per cent. This can reflect some inaccuracy of the collisional model.

### Table 1. Photometry of the q$^1$ Eri disc.

| Wavelength [\(\mu\)m] | Flux density [mJy] | Instrument | Ref. |
|------------------------|-------------------|------------|-----|
| 18                     | 315.3 ± 39.7      | AKARI      | (1) |
| 22                     | 218.1 ± 4.0       | WISE       | (1) |
| 24                     | 184.8 ± 3.8       | Spitzer/MIPS | (1) |
| 25                     | 201.1 ± 26.1      | IRAS       | (1) |
| 60                     | 617.4 ± 80.3      | IRAS       | (1) |
| 70                     | 896.2 ± 26.9      | Herschel/PACS | (1) |
| 90                     | 904 ± 60          | AKARI      | (4) |
| 100                    | 897.1 ± 26.9      | Herschel/PACS | (1) |
| 160                    | 653.9 ± 31.8      | Herschel/PACS | (1) |
| 250                    | 312.3 ± 25.6      | Herschel/SPIRE | (1) |
| 350                    | 179.9 ± 14.6      | Herschel/SPIRE | (1) |
| 500                    | 78.4 ± 9.8        | Herschel/SPIRE | (1) |
| 850                    | 30.3 ± 4.1        | JCMT/SCUBA-2 | (6) |
| 870                    | 39.4 ± 4.1        | APEX/LABOCA | (3) |
| 1200                   | < 17              | SIMBA/SEST | (2) |
| 6800                   | 0.093 ± 0.017     | ATCA       | (5) |

### References.

1. Based on data from the DUNES Archive at Centro de Astrobiología (Eiroa et al. 2013). 2. Schütz et al. (2005). 3. Liseau et al. (2008). 4. Yamamura et al. (2010). 5. Ricci et al. (2015b). 6. Holland et al., in preparation.
Table 2. Parameters of the two-component model shown in Fig. 3.

| Region | Range | $a_{\text{max}}$ | $\epsilon_{\text{max}}$ | Material | Incl. | Optical depth | $M_{\text{out}}$ | $M_{\text{disc}}$ | Age |
|--------|-------|------------------|-----------------------|----------|-------|--------------|----------------|----------------|-----|
| Inner  | 3–10  | 75–125           | 0.05                  | 30% silicate + 70% ice | 70    | $1 \times 10^{-4}$ | $1.5 \times 10^{-5}$ | 3.4 (95)       | 1.3 |
| Outer  |       |                  |                       |          |       | $1 \times 10^{-3}$ | $1.7 \times 10^{-2}$ | 8.17 (167)     |     |

Notes. (a) Radial extent of the planetesimal belts; (b) radius of the largest planetesimals; (c) maximum eccentricity of the planetesimal orbits; (d) dust material; (e) disc inclination from face on; (f) optical depth at the centre of the planetesimal belts (at the end of the simulation); (g) disc mass including grains up to 1 mm in radius (at the end of the simulation); (h) initial mass in parentheses and end mass of the whole planetesimal disc (bodies up to $a_{\text{max}}$ in radius); (i) simulation time.

Also, the modelled SED predicts submm and mm flux densities to be by a factor of 2–3 lower than those measured by LABOCA, SCUBA-2, and ATCA. Since the images from SCUBA-2 (Holland et al., in prep.) and LABOCA (Liseau et al. 2008) are extended eastwards, the most likely reason for the discrepancy is a background galaxy. The flux densities plotted are aperture fluxes. The peak fluxes – for instance, 20.1 ± 2.7 mJy/beam of the SCUBA-2 measurement – is more in line with the model prediction. Overall, we deem the resulting model satisfactory for the purposes of this paper.

The initial surface density of both components corresponds to 5.3 times the MMSN model. The position of the outer component is consistent with the ring-like disc found through a deconvolution of the Herschel 100 μm image by Liseau et al. (2010). They quote a surface brightness maximum at 85 au and a belt width of about 35 to 45 au. The location of the inner disc is beyond the orbit of the reported RV planet HD 10647b. Although there is a large gap between both components, the overall synthetic surface brightness profiles show no signs of a dip and are close to the observed ones. The best disc inclination is 70° (from face on), which is close to 76°, the value inferred from the HST scattered light image (K. Stapelfeldt, priv. comm.).

The planetesimal orbits have eccentricities $\leq 0.05$, which implies relatively low impact velocities in the disc and a rather depressed production of small dust. However, planets that reside within the disc can push planetesimals to more eccentric, and also inclined, orbits through secular perturbations (Mustill & Wyatt 2009). In particular, this planetary stirring is likely to operate in the inner component, which is close to HD 10647b. There is also the possibility that further, yet undiscovered, planets in the gap between both planetesimal belts enhance the eccentricities in the outer component. Higher values of the eccentricity are not excluded by our modelling since there are degeneracies between the eccentricity and other model parameters (see Sect. 4).

The dust composition determines the grain temperatures and emission properties. During the modelling process, we noticed that the ratio of the SED in the mid infrared shows a strong dependence on the ice fraction. This allows us to improve the agreement with the characteristic bump (“shoulder”) which is exhibited by the IRS spectrum in the 10 to 30 μm range. Larger fractions of ice reduce the emission of the inner component, whereas the one of the outer component remains nearly unchanged. This is due to the fact that the mid-infrared emission mostly comes from small grains (1-10 μm radius), while the far-infrared emission is produced by larger grains (> 10 μm) with an emissivity that is not strongly dependent on the chemical composition. The higher the ice fraction, the steeper the rise of the total SED. However, the distinct silicate feature around 18 μm is still well pronounced and is able to reproduce the bump seen in the IRS spectrum. A mixture of 30 per cent silicate and 70 per cent water ice for inner and outer component provides a good overall match to the SED and the surface brightness profiles.

4 DISCUSSION

To verify the scenario considered here, it will be crucial to resolve the proposed inner belt. At 0.17°-0.57′′, the inner belt would be difficult to see with Hubble due to the large inner working angle. The latest extreme adaptive optics instruments allow us to image much closer to the star. For instance, SPHERE/IRDIS on the VLT has an inner working angle of 0.15″ in its standard mode, opening up these regions to scattered light observations for the first time. We performed a test by generating scattered light radial profiles of the inner belt at 1.6 μm. We compared the profiles with the IRDIS detection limit provided by the SPHERE Exposure Time Calculator\(^2\). The surface brightness along the major axis, ~ 0.2 mJy/arcsec\(^2\), is about three orders of magnitude below the detection limit. For SPHERE/ZIMPOL with a smaller working angle at 0.55 μm, the inner belt could be traced along the minor axis where it appears brighter in polarized light, ~ 4 mJy/arcsec\(^2\). However, even in that case we are still one order of magnitude below the detection limit. This indicates a big challenge in resolving the inner belt with present-day observational facilities. However, the coming JWST might offer better chances for such a detection.

The proposed two-component scenario also implies a set of alleged planets between the inner and outer belts. The number of planets is unknown, as are their orbits and masses. Nevertheless, rough estimates can be made by assuming that the presumed planets are in nearly-circular, nearly-coplanar orbits with a uniform logarithmic spacing of semi-major axes (Fabér & Quillen 2007). The set of planets should be tightly packed dynamically to ensure that no dust-producing planetesimal belts have survived between the orbits, while the planets themselves should be at least marginally stable against mutual perturbations over the age of the system of ~ 1 Gyr. Using equations (3) and (6) of Fabér & Quillen (2007), we estimate that the cavity between ~ 10 au and ~ 80 au could be populated by 4–5 planets of at least Neptune mass, with a semi-major axis ratio between neighbouring planets of ~ 1.6 (i.e., similar to the orbital radius ratio of Earth and Mars in the Solar System). The minimum total mass of these planets would amount to ~ 0.2 Jupiter masses.

There are currently two planetary systems known to have an architecture similar to the one proposed for q\(^7\) Eri. One is our own Solar System. Another is a prominent system around HR 8799, with its four directly imaged massive planets (Marois et al. 2008, 2010), an outer massive “Kuiper belt” exterior to and

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Notes. (a) Radial extent of the planetesimal belts; (b) radius of the largest planetesimals; (c) maximum eccentricity of the planetesimal orbits; (d) dust material; (e) disc inclination from face on; (f) optical depth at the centre of the planetesimal belts (at the end of the simulation); (g) disc mass including grains up to 1 mm in radius (at the end of the simulation); (h) initial mass in parentheses and end mass of the whole planetesimal disc (bodies up to $a_{\text{max}}$ in radius); (i) simulation time.

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2 https://www.eso.org/observing/etc/
an inner debris belt interior to the planetary orbits (see, e.g., Reidemeister et al. 2009; Su et al. 2009). However, there are also fine differences between these cases. The q$^1$ Eri system is known to contain a close-in Jupiter-mass radial velocity planet whereas our Solar System harbours four terrestrial planets. Around HR 8799, no planets have been discovered so far inside the inner dusty belt. It is interesting to note that the known planet of q$^1$ Eri system is orbiting at $\sim$ 2 au, whereas the proposed inner belt must be located farther out, at 3 to 10 au. Thus, the belt was likely located outside the snow line when it formed which, assuming an ice sublimation temperature at the protoplanetary phase of 170 K (Lecar et al. 2006), must have been at $\sim$ 3.3 au from the star. This means that the planet could have comfortably formed in the zone interior to the "asteroid belt". No migration through the belt is required here – unlike in the systems such as HD 69830 where the planets and the belt are all located inside the snow line (Payne et al. 2009).

Due to numerous degeneracies, the model found in our study is by far not unique. For instance, we cannot constrain tightly a set of gas or icy giants that separates the two components, and consequently, it is unknown to what degree these would stir the components. However, we expect that at least the inner component is rather strongly affected by the known nearby giant planet HD 10647b which is on a close-in ($a_{pl}$ $\approx$ 2 au), eccentric orbit ($e_{pl}$ $\approx$ 0.2). Equation (6) of Mustill & Wyatt (2009) yields a forced eccentricity of $\sim$ 0.1 that could be imposed by HD 10647b on planetesimals at 5 au. Note that this is merely a rough estimate since only one planetary perturber is assumed, but it shows that the inner planetesimal disc may have a distinctly higher level of dynamical excitation than assumed in our model. If so, there would be a faster collisional depletion, resulting in a lower amount of material in the inner disc. However, the size of the largest planetesimals and their critical fragmentation energy are not well constrained, too. If there are larger and harder planetesimals within the disc, the collisional depletion would be slower, which might ensure that the inner system contains sufficient dust at $\sim$ 1 Gyr to explain the observations. The collisional timescales can also be prolonged if the inner disc were located farther out and/or had a larger width.

Furthermore, the slope of the assumed initial density profile of a protoplanetary disc is completely uncertain (e.g., Kuchner 2004; Raymond et al. 2005; Chiang & Laughlin 2013). Steeper profiles are preferred for in-situ formation scenarios of close-in giant planets, where the disc mass is more centrally concentrated.

The chemical composition of the dust is another crucial point. In our model, the dust contains 30 per cent silicates and 70 per cent water ice in inner and outer component. However, the inner component lies between 3 and 10 au. Since, in contrast to protoplanetary discs, the gas pressure in debris discs is negligible, ice sublimates at lower temperatures of $\sim$ 100 K (Kobayashi et al. 2008), suggesting the ice line for blackbody grains to lie at $\sim$ 10 au. Thus the presence of icy grains in the inner component is questionable. Other materials, e.g. porous silicate, for the inner component may be a better choice. Such a scenario agrees, at least qualitatively, with the compositional model of Tanner et al. (2009).

5 CONCLUSIONS

We consider a scenario that might naturally explain the two-component structure observed in many debris discs. This includes the formation of giant planets in an initially extended planetesimal disc that is still immersed in gas (protoplanetary phase). The nascent planets forming within the disc open the gap around their orbits by scattering the planetesimals away. Several planets together can generate a single broad gap and, as a consequence, the initially extended disc splits up into an inner and an outer region. After the gas dispersal, both planetesimal discs start to evolve collisionally. Even though the dust produced in collisions between planetesimals is spread over large distances by radiative and corpuscular forces, the structure of the underlying planetesimal distribution is that of a two-component disc. In this paper, a detailed collisional model involving realistic physics is used to simulate the long-term collisional evolution of a two-component disc around a solar-type star. Our conclusions are as follows:

1. From a comparison of the collisional simulations with predictions of a simplified analytic model of Wyatt et al. (2007), we show that the results are quite different. The surface density provided by the collisional simulations reveals much more material close to the star after an evolution period of 1 Gyr. The optical depth does not rise as steeply with distance from the star as predicted by the analytic model. This means that the discs evolving in a steady-state regime may be able to retain larger amounts of material in the inner region at older ages than thought before.

2. That scenario implies the presence of as yet undiscovered planets. Since it is the only scenario proposed so far for systems without significant transport (which is the case for stars of earlier spectral types), and since there are many two-component discs around such stars, this suggests the Solar System-like architecture with sets of planets between the Kuiper belts and asteroid belts may be quite common. If no planets populate the gap between both components, the only remaining explanation for the formation of a two-component disc will be that planetesimals, for whatever reason, did not form in a certain region of the disc.

3. The two-component model is able to reproduce the thermal emission of the q$^1$ Eri disc over a wide wavelength range. This is achieved with an inner planetesimal belt between 3 to 10 au and an outer one between 75 to 125 au. The initial surface density of both components is approximately five times the Minimum Mass Solar Nebula model. The belts contain objects up to 50 km in radius and the planetesimal orbits have a maximum eccentricity of 0.05. Silicate grains with 70 per cent ice content are assumed to reproduce the thermal emission properties. Due to a number of degeneracies, this is not a unique solution. To check the scenario itself and break some of the degeneracies, it would be vital to resolve the inner belt. There must also be a chance in the future to detect the expected planets.

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