Displacement amplification ratio modeling of bridge-type nano-positioners with input displacement loss

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Abstract. This paper presents an improved modeling method for bridge-type mechanism by taking the input displacement loss into consideration, and establishes an amplification ratio model of bridge-type mechanism according to compliance matrix method and elastic beam theory. Moreover, the amplification ratio of the designed bridge-type nano-positioner is obtained by taking the guiding mechanism as the external load of bridge-type mechanism. Comparing with existing methods, the proposed model is more accurate, which is further verified by finite element analysis (FEA) and experimental test. The consistency of the results obtained from theoretical model, FEA and experimental testing indicates that the proposed model can accurately predict the amplification characteristics of nano-positioners, which helps the analysis and design of bridge-type nano-positioners in practical applications.

1 Introduction

With the rapid development of nano precision motion systems in the emerging field of precision engineering (Zhang et al., 2015; Hao, 2017; Liu et al., 2016), the design and analysis of nano-positioners received extensive attentions with successful applications in micro-assembly, bio-engineering, scanning probe microscopy, and precision optical inspection. To meet the needs of high-precision applications, most nano-positioners use piezoelectric actuators as the driving component thanks to its characteristics of high stiffness, high resolution and high response speed (Zi et al., 2015; Liu et al., 2015; Ling et al., 2017). It should be pointed out that the direct output displacement of a piezoelectric actuator is about one thousandth of its own length, which usually can not meet the requirements of large working range in most cases. Amplifying mechanism is typically employed to amplify and transmit displacement, such as lever mechanism (Xing, 2015; Tang and Li, 2015; Tang et al., 2018), Scott-Russell mechanism (Tian et al., 2009), rhombic mechanism (Ling et al., 2018), bridge-type mechanism (Li and Xu, 2011; Chen et al., 2018; Clark et al., 2018). Among various amplifying mechanisms, bridge-type mechanism was widely investigated due to its characteristics of high amplification ratio, compact structure and easy processing.

To better help the mechanical design and structural optimization of bridge-type nano-positioners, researchers have proposed a variety of theoretical models on bridge-type amplification mechanism to describe the displacement amplification performance. Lobontiu and Garcia (Lobontiu and Garcia, 2003) derived the stiffness and displacement amplification model of the bridge-type mechanism based on the strain energy theory and the Cartesian second theorem, although the results are too complicated for implementations. Ma et al. (2006) considered the deformation of the hinge and derived the theoretical displacement amplification ratio of the bridge-type mechanism based on the full symmetry of the bridge-type mechanism and the virtual displacement theorem. Ye et al. (2011) used the full symmetry of the bridge-type mechanism to establish a quarter model of the mechanism, and used the flexibility matrix method to derive the amplification ratio formula. Qi et al. (2015) analyzed the deformation of the hinge and derived the displacement amplification model of the bridge-type mecha-
Figure 1. Bridge-type nano-positioner.

Figure 2. Bridge-type mechanism.

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nism based on the elastic beam theory. Kim et al. (2004) used the compliance matrix method to analyze the 3-D bridge-type mechanism. However, the above results focus on the deformation of flexure hinge, without considering the influence of the input displacement loss. In fact, it is observed that the input displacement loss does affect the amplification ratio of the bridge-type mechanism. Therefore the existing models need to be improved to fill this gap.

In this paper, a bridge-type mechanism based one-dimensional nano-positioner is studied. Based on the compliance matrix and Euler beam theory, theoretical amplification models of the bridge-type mechanism and the nano-positioner are presented by considering the input displacement loss. Meanwhile, finite element analysis (FEA) and experiments are also conducted to verify the proposed modeling method.

2 Design of the nano-positioner

The structure of the one-dimensional bridge-type nano-positioner studied in this paper is shown in Fig. 1. It mainly includes the bridge-type amplification mechanism, the guiding mechanism and motion platform. The bridge-type amplification mechanism can amplify the output displacement of the piezoelectric stack and the guiding mechanism composed of four flexible leaf springs has a symmetrical structure. Thanks to the leaf springs with characteristics of high longitudinal stiffness, low transverse stiffness and low stress concentration, the guiding mechanism can suppress the lateral parasitic displacement.

The bridge-type mechanism is composed of the input end, the output end, the flexible hinge and the bridge-type arm, as shown in Fig. 2. The displacement amplification deformation occurs at the input end and flexible hinges. Generally speaking, the straight-beam hinges are more flexible than other types of hinges of the same size. Therefore, the straight-beam hinges are used in the bridge-type mechanism in this paper. Moreover, the output end of the bridge-type mechanism is connected with the motion platform, where the platform is guided by the guiding mechanism. It is apparent that the guiding mechanism can be considered as an external load of the bridge-type mechanism.

A piezoelectric stack actuator is installed in the middle position of the bridge mechanism and connected with the input end of the bridge-type mechanism. According to the principle of triangular amplification, the output displacement of the piezoelectric stack is enlarged by the bridge-type mechanism such that the displacement is transmitted to the motion platform.

3 Modeling of the nano-positioner with input displacement loss

3.1 Modeling of bridge-type mechanism

As shown in Fig. 3a, the output force of the piezoelectric stack is applied on the input end, and the flexible hinge is deformed to achieve a large displacement output at the output end. When the piezoelectric stack moves, the input end of the bridge-type mechanism moves from points R and S to points R′ and S′, respectively, and the output end moves from point V to point V′. The input displacement of the bridge-type amplifying mechanism on one side is \( x_{in1} \), and the output displacement is \( y_{out1} \). The ideal displacement amplification is as follow:

\[
R_{amp1} = \frac{y_{out1}}{2x_{in1}} \tag{1}
\]

In practice, the bridge arm at the input end inevitably deforms and affects the displacement amplification performance of the bridge-type mechanism, as shown in Fig. 3a. The input end of the bridge-type mechanism moves from points R and S to points R′′ and S′′, respectively. The input displacement on one side is

\[
x_{in2} = x_{in1} + \Delta_{in} \tag{2}
\]

where \( \Delta_{in} \) is the one-sided deformation of the input end.
From the Eqs. (1) and (2), the displacement amplification ratio of the bridge-type mechanism considering the displacement loss at the input end can be obtained as

$$R_{\text{amp 1}} = \frac{y_{\text{out 1}}}{2(x_{\text{in 1}} + \Delta_{\text{in}})}.$$  

The bridge-type mechanism will be subjected to the external load $F_{\text{out}}$ of the guiding mechanism, where the output end will move from point $V'$ to point $V''$, as shown in Fig. 3b. Considering the input displacement loss and external load, we can obtain the displacement amplification ratio of bridge-type mechanism as

$$R_{\text{amp 1}} = \frac{y_{\text{out 1}} - y_{\text{out 2}}}{2(x_{\text{in 1}} + \Delta_{\text{in}})},$$

where $y_{\text{out 1}}$ is the displacement loss under external load.

The input end of the bridge-type mechanism under the action of piezoelectric stack driving force can be simplified into a simple supported beam with an intermediate force. According to the Euler beam theory and boundary conditions, the deflection of the beams can be obtained:

$$w(x) = \frac{F_{\text{in}}x}{48EI} \left(3l_{3}^{2} - 4x^{2}\right), 0 \leq x \leq l_{3}/2,$$

where $F_{\text{in}}$ is the input force, $I_{3} = (b_{3}h_{3}^{3})/12$ is the moment of inertia of the input end, $l_{3}, b_{3}$ and $h_{3}$ are the length, width and thickness of the simply supported beam, $E$ is the Young’s modulus.

Note that the output force of the piezoelectric stack is applied to the intermediate position ($x = l_{3}/2$) of the input end, where the deformation of the simply supported beam can be regarded as the displacement loss, with

$$\Delta_{\text{in}} = \frac{F_{\text{in}l_{3}^{2}}}{48EI_{3}} \left[3l_{3}^{2} - 4\left(\frac{l_{3}}{2}\right)^{2}\right] = \frac{F_{\text{in}l_{3}^{2}}}{48EI_{3}}.$$

Thanks to the symmetrical structure, the model of the bridge-type amplification mechanism can be obtained by analyzing the 1/4 structure. As shown in Fig. 4, $F_{A_x} = F_{B_x}$ and $F_{A_y} = F_{B_y}$ are two pairs of reaction forces applied to the hinges $A$ and $B$. The following results can be obtained from the force balance relationship:

$$F_{A_x} = F_{B_x} = F_{x} = \frac{F_{\text{in}}}{2},$$

$$F_{A_y} = F_{B_y} = F_{y} = \frac{F_{\text{out}}}{2},$$

$$M_{A} = M_{B} = M = \frac{F_{x}l_{2} - F_{y}l_{1}}{2},$$

$$\sin a = \frac{l_{2}}{l_{a}}, \quad \cos a = \frac{l_{1}}{l_{a}},$$

where $l_{1}$ is the length of the vertical arm, $l_{2}$ is the vertical distance between the hinges, $l_{a}$ is the distance between the hinges, $a$ is the deflection angle between the two hinges.

In this study we only consider the planar deformation of the flexible hinge. Based on the compliance matrix method (Koseki et al., 2002), the straight-beam flexible hinge output
can be simplified to

\[
\begin{bmatrix}
\Delta x_l \\
\Delta y_l \\
\Delta a
\end{bmatrix} =
\begin{bmatrix}
\frac{l}{Ebt} & 0 & 0 \\
0 & \frac{4l^3 + l}{3Ebt^3} + \frac{6l^2}{6l^2 + Gbt} & 0 \\
0 & \frac{12l}{Ebt^3} & \frac{F_x}{F_y}
\end{bmatrix}
\begin{bmatrix}
F_x \\
F_y \\
M
\end{bmatrix},
\]  

(11)

where \( \Delta x_l \) and \( \Delta y_l \) are deformations of the flexible hinge in the plane along the \( x \) and \( y \) directions respectively, \( \Delta a \) is the rotation angle of the flexible hinge around the \( z \) axis, \( E \) is the Young’s modulus of the material, \( G \) is the shear modulus, \( l \), \( t \) and \( b \) are the length, width and thickness of the hinge.

To further study the deformation of the bridge-type mechanism, we consider tensile deformation of the bridge arm during the amplification process

\[
\Delta l_a = \frac{(F_{Bx} \sin a + F_{By} \cos a)l_a}{EA_a},
\]

(12)

where \( A_a \) is the cross-sectional area of the bridge arm connecting the two hinges.

Input displacement of 1/4 structure is considered in the following parts: deformation of flexible hinges \( A \) and \( B \), rotation and extension of bridge arm \( AB \), displacement loss at the input end, which results in

\[
\Delta x = 2\Delta x_l + l_a \sin a \Delta a + \Delta l_a \cos a + \Delta_{in}.
\]

(13)

Similarly, the output displacement of 1/4 structure is considered with the following factors: deformation of flexible hinges \( A \) and \( B \), rotation and extension of bridge arm \( AB \), which is represented as

\[
\Delta y = 2\Delta y_l + l_a \cos a \Delta a + \Delta l_a \sin a.
\]

(14)

Substituting Eqs. (6), (10), (11) and (12) into Eq. (13), we can obtain the input displacement as

\[
\Delta x = \left( \frac{2l}{Ebt} + \frac{l^2}{EA_{Ala}} + \frac{2l^3}{48EI_5} + \frac{6l^2}{Ebt^3} \right) F_x
\]

\[
+ \left( \frac{6l^2l_2 - 6l_2l_1}{Ebt^3} + \frac{l_1l_2}{EA_{Ala}} \right) F_y.
\]

(15)

Similarly, we can obtain the output displacement by substituting Eqs. (10), (11) and (12) into Eq. (14):

\[
\Delta y = \left( \frac{6l^2l_2 + 6l_1l_2}{Ebt^3} + \frac{l_1l_2}{EA_{Ala}} \right) F_x
\]

\[
+ \left( \frac{8l^3 - 18l_2^2}{3Ebt^3} + \frac{2l}{Gbt} + \frac{l_2^2}{EA_{Ala}} \right) F_y.
\]

(16)

When the external load is applied, the amplification ratio of the bridge-type mechanism considering the input displacement loss can be obtained as

\[
R_{amp} = \frac{2\Delta y}{2\Delta x}
\]

\[
= \left( \frac{6l^2l_2 + 6l_1l_2}{Ebt^3} + \frac{l_1l_2}{EA_{Ala}} \right) F_x
\]

\[
+ \left( \frac{8l^3 - 18l_2^2}{3Ebt^3} + \frac{2l}{Gbt} + \frac{l_2^2}{EA_{Ala}} \right) F_y.
\]

(17)

If the external load \( F_y = 0 \), the amplification ratio of the bridge-type mechanism can be written as

\[
R'_{amp} = \frac{6l^2l_2 + 6l_1l_2}{Ebt^3} + \frac{l_1l_2}{EA_{Ala}},
\]

(19)

which is different from the result considering the impact of input displacement loss as shown in Eq. (18). We will further verify this discrepancy with the FEA method in Sect. 4.

3.2 Modeling of guiding mechanism

As shown in Fig. 5a, the guiding mechanism in the nano-positioner is the external load of the bridge-type amplification mechanism. In order to deliver large displacement while reducing parasitic displacement in \( x \) direction, the guiding mechanism employs four long flexible leaf springs of the same size, with a symmetrical arrangement.

The long flexible leaf spring can be treated as a tension spring, as shown in Fig. 5b. The end point is subjected to load \( F_a = [F_{aq}, F_{sq}, M]^T \). Since the deformation range of the nano-positioner is much smaller than the size of the long flexible leaf spring, the effect of tensile force \( F_{aq} \) on the rotation and deflection can be neglected, where the rotation angles produced by \( F_{sq} \) and \( M_q \) are

\[
\theta_{aq} = \frac{F_{sq} l_2}{2EI_5}, \quad \theta_{aq} M_q = -M_q l_2.
\]

(20)
The deflections induced by $F_{sq}$ and $M_q$ are

$$w_{sq} = \frac{F_{sq}l_3^3}{3EI_s}, \quad w_M = \frac{Mql_3^2}{2EI_s},$$

where $I_s = (bs^3t_s^3)/12$ is the moment of inertia of the flexible leaf spring, $t_s$, $b_s$, $l_s$ are the thickness, width and length of the leaf spring respectively.

Now that recall the boundary conditions that $w_p = 0$, $\theta_p = 0$, and $\theta_q = 0$. The deflection of single leaf spring can be obtained by superposition from Eqs. (20) and (21):

$$w_q = \frac{F_{sq}l_3^3}{12EI_s}.$$ 

(22)

The stiffness of guiding mechanism is

$$k_s = \frac{F_{out}}{w_q} = \frac{F_{sq}}{w_q} = 4k_1 = \frac{4Eb_sbs^3}{l_s^3},$$

(23)

where $s_y$ is the output displacement of the guiding mechanism under the force $F_{out}$ and $k_1$ is the stiffness of a single flexible leaf spring.

### 3.3 Modeling of the nano-positioner

According to the symmetry of the bridge-type mechanism, the input and output displacements are

$$x_{in} = 2\Delta x,$$

(24)

$$y_{out} = s_y = 2\Delta y.$$ 

(25)

From Eqs. (7), (8), (9), (11), (16), (23) and (25), the output displacement of the bridge-type nano-positioner can be derived as

$$y_{out} = \frac{6l^2_{l_2} + 6ll_{l_2}l_2 + l_1l_2}{Eb^3} + \frac{l_1l_2}{EA_a l_a}$$

(26)

$$\left[1 - \left(\frac{8l^3 - 18ll_1}{3Eb^3} + \frac{2l}{Gb^3} + \frac{l_1^2}{EA_a l_a}\right)\frac{4Eb^3}{l_s^3}\right]F_{in}.$$

### Finite element simulation and verification

To verify the model proposed in this paper, FEA simulations will be provided in this section. The material of the nano-positioner is aluminum alloy Al-7075.
Table 2. The results of different methods and the FEA.

| Category                     | Amplification ratio | Relative error |
|------------------------------|---------------------|----------------|
| Eq. (18)                     | 8.00                | 2.56 %         |
| Eq. (19)                     | 8.16                | 4.62 %         |
| Model in Ma et al. (2006)    | 7.18                | 7.95 %         |
| Model in Ye et al. (2011)    | 7.55                | 3.21 %         |
| Model in Qi et al. (2015)    | 8.20                | 5.13 %         |
| FEA result                   |                     | 4.1 Finite element verification of the bridge-type mechanism

We first conduct simulations of the bridge-type mechanism without external load, where the structure parameters are shown in Table 1.

The case of 20 µm of input displacement is depicted in Fig. 6, where the displacement amplification ratio of the bridge-type mechanism is also obtained and compared with existing results in the literature, as shown in Table 2. It is clearly seen that the model proposed in the present work can more accurately describe the mechanism amplification ratio of the bridge-type mechanism, compared with representative results such as Ma et al. (2006); Ye et al. (2011) and Qi et al. (2015), thanks to the consideration of the input displacement loss. The importance of considering the input displacement loss can also be seen from the comparison of Eqs. (18) and (19) in Table 2.

It is also interesting to check the influence of the input structure parameters ($l_3$, $h_3$) on the amplification ratio of the bridge-type mechanism, which is shown in Fig. 7 by recalling Eq. (18).

In order to verify the influence of the input end displacement loss on the amplification performance of the mechanism, the displacement amplification under different structural parameters ($l_3$, $h_3$) was simulated. The analysis results are shown in Fig. 8, which shows the necessity of considering the input displacement loss in the modeling of the bridge-type mechanism. As the length $l_3$ of the input end increases, the displacement loss of the input end of the bridge-type mechanism increases and the displacement amplification ratio decreases. As the thickness $h_3$ of the input end increases, the input end loss of the bridge-type mechanism is reduced and the displacement amplification ratio is increased. The
consistency between the simulation results and the calculation results further validates the effectiveness of the proposed modeling method.

4.2 Finite element verification of bridge-type nano-positioner

The FEA simulations are also conducted to verify the amplification ratio model of the nano-positioner as described by Eq. (27), where the structural parameters are listed in Table 3. As depicted in Fig. 9, the deformation result of the bridge-type nano-positioner with an input displacement of 10 µm is simulated. It is also seen from Table 4 that the result of Eq. (27) agrees well with that of FEA, where the relative error is only 4.16%.

5 Experimental verification

The proposed modeling method and the simulation results are also verified by experiments, where the nano-positioner is machined by the wire-cutting machining method according to the structural parameters in Table 3. The overall ex-

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**Figure 8.** Influence of structure parameters on amplification ratio. (a) The influence of $l_3$ on the amplification ratio. (b) The influence of $h_3$ on the amplification ratio.

**Figure 9.** FEA simulation of the nano-positioner.

**Table 3.** Structure parameters of the nano-positioner.

| Parameters | Value |
|------------|-------|
| $b$ (mm)   | 14.5  |
| $l_1$ (mm) | 13    |
| $h_3$ (mm) | 5     |
| $l_2$ (mm) | 13.1  |
| $l_3$ (mm) | 21    |
| $l$ (mm)   | 0.4   |
| $l_2$ (mm) | 1.8   |
| $h_3$ (mm) | 14.5  |
| $b_3$ (mm) | 5     |
| $A_d$ (mm²)| 72.5  |

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Table 4. FEA verification of bridge-type nano-positioner.

| Category | Amplification ratio | Relative error |
|----------|---------------------|----------------|
| Eq. (27) | 7.26                | 4.16 %         |
| FEA result | 6.97                |                |

Figure 10. Experimental setup of the nano-positioner system.

Experimental apparatus is shown in Fig. 10, where the nano-positioner is driven by NAC14 piezoelectric stack though a high bandwidth voltage amplifier.

In the experiment, the slope voltage signal of 0–50 V is applied to the PZT actuator, where the input and output displacement of the nano-positioner are captured by an laser interferometer and plotted in Fig. 11. According to the experimental results, the actual displacement amplification ratio of the nano-positioner is 7.10, which is close to the calculated result of 7.26 and FEA simulation result of 6.97. As shown in Table 5, the proposed model can effectively predict the amplification performance of the bridge-type nano-positioner by considering the impact of input end displacement loss.

6 Conclusions

In this paper, an improved model was developed to describe the displacement amplification of the bridge-type mechanism, by considering the displacement loss of the input end, which was also extended to the analysis of displacement amplification ratio of bridge-type nano-positioner by regarding the guiding mechanism as the external load of the bridge-type mechanism. FEA simulations and real time experiments were provided to comprehensively evaluate the proposed method. Comparative studies and experiments indicate that the proposed method can better capture the amplification performance for such systems, which can be potentially used in the design and optimization of bridge-type nano-positioners.

Table 5. Displacement test of the nano-positioner.

| Category | Amplification ratio | Relative error |
|----------|---------------------|----------------|
| Eq. (27) | 7.26                | 2.2 %          |
| FEA      | 6.97                | 1.8 %          |
| Experimental result | 7.1                |                |

Competing interests. The authors declare that they have no conflict of interest.

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