A Formula to Predict the Magnitude of Achilles Tendon Lengthening Required to Correct Equinus Deformity

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Significance of the Study

• Achilles tendon lengthening is a frequently used surgical treatment for equinus deformity.
• This study describes a mathematical formula that allows preoperative determination of the amount of Achilles tendon lengthening.
• Calculating the amount of lengthening before surgery will allow more accurate determination of the correct tendon length and will reduce the size of the surgical incision.

Keywords
Achilloplasty · Achilles tendon lengthening

Abstract
Objectives: Achilles tendon lengthening (ATL) is one of the most commonly performed procedures in paediatric orthopaedic surgery. An appropriate adjustment of the amount of ATL is crucial to avoid insufficient or excessive lengthening. However, there is currently no effective method to preoperatively calculate the tendon length needed for equinus deformity correction. Thus, in this study we evaluated the accuracy of a calculation using a mathematical model based on the law of cosines.

Methods: A total of 16 feet of 14 patients who were scheduled for ATL surgery due to equinus deformity were included in the study. ATL surgery was performed using a standard Z-plasty technique. Calculation of the amount of ATL using the law of cosines, and assessments of intraoperative lengthening of the tendon, were performed in a double-blind manner. The extent of lengthening resulting from the two methods was then compared.

Results: The mean ATL determined intraoperatively was 23.67 ± 8.7 mm, and that obtained using the cosine-based method was 22.49 ± 8.6 mm. Thus, the new method showed excellent statistical agreement with the actual lengthening performed during surgery.

Conclusions: The required dimension of ATL can be calculated preoperatively using the mathematical formula presented here. The advantages of this approach are that it allows accurate tendon lengthening and reduces the size of the surgical incision.

Introduction

Equinus deformity, defined as the inability to dorsiflex the foot beyond plantigrade [1], is a common problem in children with spastic cerebral palsy [2]. Surgical treat-
ment of equinus deformity consists of Achilles tendon lengthening (ATL) or gastrocnemius recession [3]. The choice between the two methods depends on the results of the Silfverskiöld test [4].

ATL is usually performed on patients with equinus contracture and a negative Silfverskiöld test. Among the techniques often used for ATL are two- or three-cut percutaneous tenotomies and Z-lengthening [1, 5, 6]. However, whereas the lengthening technique has been well studied, the possibility of preoperative determination of the appropriate amount of lengthening has not been considered.

In current practice, the magnitude of ATL is usually established intraoperatively, by positioning the patient’s foot at the desired angle of dorsiflexion and then suturing the tendon in the lengthened position. Because determination of the exact tendon length is often difficult, insufficient or excessive ATL may be a major surgical complication. Insufficient lengthening may lead to residual equinus deformity, and excessive lengthening to crouch gait, which occurs due to muscle weakness and is difficult to treat [4]. Furthermore, in the standard Z-plasty technique, the extent of incision cannot be adjusted according to the extent of lengthening, as sufficient tendon contact may not be achieved. A precise ATL procedure is therefore essential [7].

Our hypothesis is that the required magnitude of ATL can be calculated according to the amount of contracture using the law of cosines. The aim of the study was to develop a mathematical equation that determines the appropriate amount of ATL preoperatively.

**Patients and Methods**

Equinus deformity was diagnosed in 16 feet of 14 cerebral palsy patients (8 boys and 6 girls) and open Z-plasties were planned. Lateral ankle X-ray images with the knee extended and the ankle in neutral dorsiflexion were used. The extent of lengthening (ATL) required was calculated using the above-cited formula as the calculated amount of contracture and amount of lengthening (PAL), and the ATL performed amount of lengthening (PAL), and the ATL was calculated using the be simplified as ATL = \(\sqrt{2d^2(1 – \cos(\alpha))}\).

In this study, the measurements and calculations were made by a surgeon blinded to the amount of lengthening performed during surgery. The intraoperatively determined ATL is referred to as the performed amount of lengthening (PAL), and the ATL calculated using the above-cited formula as the calculated amount

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**Calculations**

The rotational centre of the ankle in the sagittal plane (RCA) was designated based on the centre of a circle containing the arc of the talocrural joint surface [8], and the Achilles tendon insertion (AI) as the junction of the posterior border of Kager’s triangle with the calcaneus [9]. The distance between the RCA and the AI was defined as “d” (Fig. 2), the amount of change in the angle between the foot and ankle between before and after surgery as “\(\alpha\)” (Fig. 3), and the amount of AI displacement after lengthening which is also the amount of ATL as “x” (Fig. 3). It was assumed that during ankle plantar dorsiflexion the AI moves in a circle centred at the RCA (Fig. 3).

If d and \(\alpha\) are measured, then the amount of ATL (x) can be calculated using the simplified as ATL = \(\sqrt{2d^2(1 – \cos(\alpha))}\). In this study, the measurements and calculations were made by a surgeon blinded to the amount of lengthening performed during surgery. The intraoperatively determined ATL is referred to as the performed amount of lengthening (PAL), and the ATL calculated using the above-cited formula as the calculated amount.
Calculation of the Amount of Achilles Tendon Lengthening

The distribution of the groups was determined using the Kolmogorov-Smirnov test, and group differences were assessed using the independent-samples t test. Absolute agreement in a two-way mixed random-effects model was used to compute the intraclass correlation coefficient (ICC) based on a 95% confidence interval (CI). An ICC ≤ 0.5 indicated a poor fit, an ICC of 0.5–0.75 a medium fit, an ICC of 0.75–0.90 a good fit, and an ICC ≥ 0.90 an excellent fit.

Results

The mean patient age at the time of surgery was 9 ± 3.1 years (range: 6–18). The mean magnitude of lengthening in the PAL and CAL groups was similar (p = 0.728): 23.67 ± 8.7 and 22.49 ± 8.6 mm, respectively. The two groups also showed excellent agreement in the extent of lengthening (ICC = 0.953; 95% CI: 0.861–0.984) (Table 1).

Discussion

Equinus is a common deformity in children with cerebral palsy [1]. In those with a fixed equinus contracture, it is often treated by ATL. While percutaneous procedures are relatively non-invasive, with minimal surgical scarring and morbidity and few wound-healing problems [6], the lack of a method to determine the amount of lengthening required preoperatively increases the risk of over- or underextension of the tendon [5]. Open surgery allows the amount of tendon lengthening to be adjusted during surgery and is therefore not hindered by the inability to determine the required tendon length prior to the procedure. Sufficient durability during tendon repair after lengthening is typically achieved with 3–4 cm of tendon contact surface area [11].

Since a shorter-than-necessary incision will not allow adequate contact between the tendon limbs, with the standard technique, a long longitudinal incision is made regardless of the extent of the deformity, due to concerns regarding an insufficient tendon contact surface area. The ability to determine the required amount of ATL before surgery will improve the safety of minimally invasive ATL.

Fig. 2. Identification on X-ray of the rotational centre of the ankle in the sagittal plane (RCA). AI, Achilles tendon insertion; d, distance between the RCA and the AI.

Fig. 3. Displacement of the AI within a circle centred around the RCA during plantar dorsiflexion of the ankle. AI, Achilles tendon insertion; RCA, rotational centre of the ankle in the sagittal plane; d, distance between the RCA and the AI; α, amount of change in the equinus between before and after surgery; x, the extent of Achilles tendon lengthening.
procedures. For example, a 5-cm incision will be sufficient for a patient in whom 2 cm of tendon lengthening and 3 cm of tendon contact are planned. Alternatively, surgery can be performed in a minimally invasive manner via two incisions spaced 5 cm apart.

In this study, because our newly devised formula was untested in practice, the amount of lengthening was set using our standard technique and the corresponding calculation was performed after surgery. Analysis of the PAL and CAL data revealed an excellent correlation. Preoperative calculation of the amount of ATL may allow for adequate correction through minimal incision, instead of an incision along the Achilles tendon. The smaller incision will reduce surgical scarring, morbidity, and wound healing problems while shortening the surgical time. Although our calculation cannot be expected to yield an absolute result, as it is a purely geometric approach to a biological problem varying in severity, it does allow preoperative prediction of the magnitude of ATL.

A limitation of this calculation is that it is not a simple mathematical operation, but requires the use of a cosine table. To simplify the calculation, the amount of ATL required for different degrees of equinus contracture and distances “d” is presented in Table 2.

**Table 1.** Correlation between the performed amount of lengthening (PAL) and the calculated amount of lengthening (CAL)

|                         | Intraclass correlation | 95% confidence interval | F test with true value 0 |
|-------------------------|------------------------|-------------------------|-------------------------|
|                         |                        | lower boundary | upper boundary | value | df1 | df2 | p    |
| PAL-CAL                | 0.953                  | 0.861        | 0.984        | 23.414 | 14  | 14  | <0.001 |

**Table 2.** Amount of tendon lengthening (mm) required for various degrees of equinus contracture and various distances “d”

|            | 10° | 20° | 30° | 40° | 50° | 60° | 70° | 80° | 90° |
|------------|-----|-----|-----|-----|-----|-----|-----|-----|-----|
| 10 mm      | 1.74| 3.47| 5.18| 6.84| 8.45| 10.00| 11.47| 12.86| 14.14 |
| 20 mm      | 3.49| 6.95| 10.35| 13.68| 16.90| 20.00| 22.94| 25.71| 28.28 |
| 30 mm      | 5.23| 10.42| 15.53| 20.52| 25.36| 30.00| 34.41| 38.57| 42.43 |
| 40 mm      | 6.97| 13.89| 20.71| 27.36| 33.81| 40.00| 45.89| 51.42| 56.57 |
| 50 mm      | 8.72| 17.36| 25.88| 34.20| 42.26| 50.00| 57.36| 64.28| 70.71 |
| 60 mm      | 10.46| 20.84| 31.06| 41.04| 50.71| 60.00| 68.83| 77.13| 84.85 |
| 70 mm      | 12.20| 24.31| 36.23| 47.88| 59.17| 70.00| 80.30| 89.99| 98.99 |
| 80 mm      | 13.94| 27.78| 41.41| 54.72| 67.62| 80.00| 91.77| 102.85| 113.14|
| 90 mm      | 15.69| 31.26| 46.59| 61.56| 76.07| 90.00| 103.24| 115.70| 127.28|

**Conclusions**

We developed a formula that determines the amount of ATL needed to correct an equinus contracture. However, further studies are needed to evaluate the clinical outcomes of patients treated with ATL as predicted using this formula.

**Statement of Ethics**

This prospective study was approved by the Institutional Review Board of our hospital.

**Disclosure Statement**

The authors have no conflicts of interest to disclose.
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