In this paper, a microwave frequency comb (MFC) is generated from a semiconductor laser subject to optical injection from a commercial small form-factor pluggable (SFP) optical module which is modulated by an arbitrary periodic signal. A sinusoidal signal or square wave signal is employed as the arbitrary periodic signal instead of the electric pulse signal adopted in the former references. When the frequency of the modulated signal is 1 GHz, the MFC with a maximal bandwidth of 15 GHz can be obtained. In addition, taking a sinusoidal signal as an example, the influence of the injection optical power to the slave laser and the modulation frequency of the optical module on the generation of the MFC is analyzed in detail. Finally, the results of MFC generated with a square wave signal injection are presented. The experimental results of this paper provide an important reference for the practical applications of MFC.

1. Introduction

With the external disturbances such as external optical injection, optical feedback, or opto-electric feedback, a semiconductor laser can produce some nonlinear dynamic phenomena, including period one oscillation [1, 2], period-doubling oscillation, quasiperiod oscillation, and chaos [3–8]. In addition, a semiconductor laser can also generate microwave frequency comb (MFC) under the external optical injection. MFC is widely used in frequency measurement, radar detection, frequency conversion, radio-over-fiber (RoF) transmission system, and other fields due to the advantages of multiple continuous microwave signals, flexible and adjustable comb line spacing, wide frequency range, and high comb spacing precision [2, 9–11]. Therefore, generation of stable and high-quality MFC has become a research hotspot.

Some methods of generating MFC have been reported up to now. The MFC signal with a bandwidth of 3 GHz was generated by using the subharmonic frequency locked state generated by the opto-electric feedback of semiconductor laser [12]. But the comb spacing of the frequency comb was not strictly equal. Moreover, the noise of noncomb component was obvious. By injecting the regular optical pulse generated by opto-electric feedback of semiconductor laser into the other semiconductor lasers, the MFC signal was generated with an amplitude of ±5 dB and bandwidth of 20 GHz [13, 14]. However, the signal was unstable, and the comb line spacing was small. By adopting the nonlinear effect of STM tunnel junction, the generation of the MFC signal with up to 200 harmonics was realized. The central frequency of the highest harmonic is 14.85 GHz. Yet there are some disadvantages such as difficult to tune the comb spacing and large phase noise [15–17]. In addition, the numerical simulations and experiments have been presented for the generation of tunable MFC signal by semiconductor laser subject to optical injection, in which the master laser is modulated by a periodic electric pulse signal [18–20].
In this paper, a tunable MFC signal is obtained by using an external optical injection semiconductor laser. The master laser is a commercial SFP optical module modulated by a periodic electronic signal not just a periodic electric pulse signal used in [20]. The modulation signal in this experiment is the sinusoidal signal produced by a RF signal generator or the square wave signal produced by a bit-error-rate tester (BERT). As the master laser, in order to reduce the cost and the complexity of the setup, we use a commercial optical module which is cheap, simple, and easy to be modulated.

2. Experimental Setup

The experimental setup of the tunable MFC produced by a semiconductor laser subject to the optical injection from a SFP optical module modulated by a sinusoidal signal is presented in Figure 1. The master laser is a 2.5 Gb/s small form-factor pluggable (SFP, Finisar) optical module, yet the slave laser is a distributed feedback (DFB) semiconductor laser without a build-in optical isolator. The optical power and central wavelength of the slave laser are controlled by the current source circuit and the temperature control circuit, respectively. The SFP module generates an optical signal that changes with the modulation of a sinusoidal signal from a RF signal generator (SG, IFR 2042, 5.4 GHz). After being amplified by erbium-doped fiber amplifier (EDFA), the light enters the variable optical attenuator (VOA) to adjust the injected optical power. A polarization controller (PC) is adopted to adjust the polarization state. Then, the light enters the slave laser through the optical circulator (OC) to generate a new optical signal utilizing nonlinear interaction. A 50:50 optical coupler is adopted to divide light into two beams. One beam enters a photodetector (PD, Picometrix, PT-40D/AC) with a bandwidth of 40 GHz to convert the optical signal into electrical signal. The output electrical signal is gathered by the electrical spectrum analyzer (ESA, Rohde & Schwarz, FSEK20, 40 GHz). The other beam enters the optical spectrum analyzer (OSA, Anritsu, MS9710C) to analyze the optical spectrum.

The frequency range of the sinusoidal signal generated from the signal generator is changed from 0.5 GHz to 5.4 GHz in this experiment. The SFP is an optical module that meets the dense wavelength division multiplexing (DWDM) wavelength requirements. The actual output wavelength is 1549.76 nm. In order to adjust the injected optical power for a large range, the EDFA is necessary. The output power of the SFP is small, but the power can be amplified to 11.3 dBm by EDFA working under the automatic power control (APC). The VOA is employed to adjust the optical power injecting into the slave laser with an initial attenuation coefficient of 11 dB. The bias voltage of the photodetector with a transimpedance amplifier is +4 V, yet the voltage for the transimpedance amplifier is +3.3 V. For this experiment, the optimal MFC signal is obtained by adjusting the frequency of the sinusoidal signal from the signal generator, the PC, and the VOA.

3. Effect of the Injection Optical Power on MFC

The initial frequency of the signal generator is 1 GHz with an amplitude of +0.7 V. The attenuation coefficient of the VOA is between 11 dB and 25 dB with an attenuation step of 1 dB. When the attenuator coefficient is 11 dB, the obtained MFC is shown in Figure 2(a). The comb line spacing of the MFC is equal to the frequency of the modulation signal, which is 1 GHz. The bandwidth of MFC can be determined by the electrical spectrum analyzer as follows. Firstly, the function of electrical spectrum analyzer to find the peak value is used to directly locate the component with the highest power for the frequency comb. The frequency of the component is 3 GHz, and the power is −27.95 dBm, which is the third comb line of the MFC. In this paper, the bandwidth for the MFC is defined as 10 dB [20], that is, the maximum power value minus 10 dBm. Then, the MFC component within this range is the bandwidth. Accordingly, an isoline with a power of −27.95 dBm is drawn to determine the upper bound. Secondly, an isoline with the power of −37.95 dBm is drawn to determine the lower bound. It can be seen from Figure 2(a) that there are 15 comb line components between the two power contour lines. Therefore, the bandwidth of the MFC is 15 GHz. The peak power difference for each comb line is small. Hence, the MFC signal quality is good. Although there is a frequency component greater than 15 GHz, the signal power is lower than −37.95 dBm, which is not considered in the bandwidth.

The MFC signal is shown in Figure 2(b) when the attenuation coefficient of the VOA is set to 20 dB. The frequency of the modulation signal is 1 GHz; hence, the frequency of the generated MFC signal is an integral multiple of 1 GHz, that is, from 1 GHz and 2 GHz to 11 GHz. Except these frequencies, noise appears. It can be seen that there is a lot of noise at the bottom of some frequency comb lines. The frequency comb with the high frequency part is almost submerged by noise. The signal quality is not as good, as shown in Figure 2(a), but the MFC with a wide spectrum...
can still be obtained. According to the above method of bandwidth determination, it can be concluded that the bandwidth of the MFC is 11 GHz for this case.

For this experiment, we also measured the optical spectrum of the optical signal generated from SL after optical injection. Figure 2(c) is the optical spectrum when the attenuation coefficient of VOA is 11 dB. Curve A is the optical spectra of the optical signal generated from SL with the injection from SFP module. Curve B denotes the optical spectrum of the SFP module. It can be seen that the central wavelength of the optical signal generated from SL after optical is equal to that of the SFP module. That is to say, when the central wavelength of the master laser and the slave laser is equal, the MFC can be obtained. Figure 2(d) is the optical spectrum of the VOA when the attenuation coefficient is 20 dB. It can be seen that the optical spectrum hardly changes with the increasing attenuation coefficient.

The injection optical power from the SFP module decreases gradually by adjusting the attenuation of VOA. The bandwidth of the MFC changes with the attenuation coefficient, as shown in Figure 3. When the attenuation coefficient is from 11 dB to 13 dB or from 24 dB to 25 dB, the bandwidth of the MFC does not change. When the attenuation coefficient is from 14 dB to 24 dB, the MFC bandwidth presents a general decreasing trend with the increasing attenuation coefficient. Therefore, the bandwidth of the MFC generated in this experiment generally decreases with the decrease in the output power of the SFP module, but the overall fluctuation is not big.

4. Effect of Modulation Frequency on MFC

During this section, the attenuation coefficient of VOA is maintained at 11 dB. Figure 4(a) shows the generated MFC.
when the modulation frequency from the signal generator is 0.5 GHz. It can be seen that the comb line spacing of the MFC is equal to the frequency of the modulation signal, i.e., 0.5 GHz. Compared with the result of 1 GHz modulation frequency in Figure 2(a), when the modulation frequency is 0.5 GHz, the power of the low-frequency base part increases, so the quality of the obtained MFC decreases. The bandwidth for the MFC shown in Figure 4(a) is 7 GHz. The obtained MFC is shown in Figure 4(b) when the output frequency of the signal generator is 3.5 GHz. The comb line spacing is 3.5 GHz, which equals to the sinusoidal signal modulation frequency. However, the frequency comb of the high frequency part disappears. As shown in Figure 4(b), the MFC whose overall base is flat is better than the result presented in Figure 4(a). The bandwidth for the MFC shown in Figure 4(b) is 14 GHz.

The relationship between the bandwidth of the MFC and the modulation frequency is displayed in Figure 5. With the increasing modulation frequency, the bandwidth of MFC is generally increasing. When the modulation frequency is between 1 GHz and 2 GHz, the bandwidth decreases slightly. The quality of the MFC is not very good. Generally speaking, when the range of the modulation frequency is from 2.5 GHz to 5 GHz, the bandwidth begins to increase. Moreover, not only the noise is relatively small and the comb line is clean but also the power distribution of each comb line is relatively uniform.

5. MFC Generated with Square Wave Signal Modulation

In order to illustrate that a MFC signal can be generated from a semiconductor laser subject to optical injection from a SFP module modulated by arbitrary periodic signal, a square wave signal is employed as the modulated signal.
Figure 5: Effect of modulation frequency on MFC.

Figure 6: Results of the MFC generated by the square wave signal modulation. (a) and (c) are the 0.5 GHz and 1 GHz square wave signals, respectively. (b) and (d) are the generated MFC with the modulation of 0.5 GHz and 1 GHz square wave signals, respectively.
During this experiment, a bit-error-rate tester (BERT, Anritsu, MP1632A, 3.2 Gb/s) is utilized to generate a square wave signal. By the way, a bit-error-rate tester is generally arranged to generate the pseudorandom bit sequence. The specific setting is to utilize the pattern setting function in the pattern editor menu of the BERT. The data output from the pulse pattern generator (PPG) of the BERT is the square wave signal when the running mode is selected as programmable pattern (PRGM) and set the pattern type as periodic 0 and 1. The time-domain waveform is displayed on a real-time digital oscilloscope (OSC, Tektronix, TDS7404B, 4 GHz, 20 GS/s).

The square wave signal generated by the BERT is employed to modulate the SFP module. Figure 6(a) presents the square wave signal with the output frequency of 0.5 GHz. Figure 6(b) displays the corresponding MFC signal generated by slave laser with the optical injection from SFP module with the modulation of the square wave signal. For this case, the bandwidth of MFC signal is 6 GHz. Comparing the MFC obtained this time with that obtained from the sinusoidal signal with the modulation frequency of 0.5 GHz, the bandwidth is 6 GHz and 7 GHz, respectively. Not only the difference of the bandwidth is not big but also the main characteristics of the base noise distribution, comb line, and comb line power distribution of the MFC are similar.

When the frequency of the square wave signal is 1 GHz, the results of the oscilloscope and the electronic spectra are shown in Figures 6(c) and 6(d), respectively. The comb line spacing of the MFC signal increases from 0.5 GHz to 1 GHz when the square wave signal is 1 GHz. The number of the comb lines decreases, and the power of comb lines component within the bandwidth increases. Hence, the MFC signal quality generally improves. When the frequency of modulation signal is 1 GHz, the bandwidth of the MFC signal obtained with the square wave signal and the sinusoidal signal is 15 GHz and 14 GHz, respectively. The results of the two MFC signals on the electronic spectrum analyzer are approximately the same. This is a strong proof of the argument put forward in this paper; that is, the MFC can be generated from a semiconductor laser with optical injection from a modulated SFP module by arbitrary periodic signal.

Other waveforms, such as triangle-wave signal or periodic pulse signal, can also be adopted as the modulated signal, which can be generated by arbitrary waveform generator (AWG) with high bandwidth. At present, we have no such high-bandwidth AWG in our laboratory. In future, we will conduct some experiments to generate MFC with the modulation signal produced by AWG.

6. Conclusions

In this paper, a sinusoidal signal or square wave signal is employed as a periodic signal to modulate the SFP module in order to realize the generation of the microwave frequency comb signal from the semiconductor laser with the injection from the SFP module. The proposed setup can generate stable microwave frequency comb signal in the range of 6 GHz–16 GHz. The results of this paper provide a useful reference for the practical application of the microwave frequency comb signal.

Data Availability

The data used to support the findings of this study are available from the corresponding author upon request.

Conflicts of Interest

The authors declare that there are no conflicts of interest regarding the publication of this paper.

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