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Experimental and Numerical Studies on Thermally-Induced Slip Ratcheting on a Slope

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Abstract: Mild temperature fluctuation of a material sitting on a slope may only cause a small slip, but a large number of the repeated temperature changes can amplify the magnitude of the overall slip and eventually bring an issue of structural instability. The slip accumulation starts from the minor magnitude and reaches the extensive level called “slip ratcheting”. Experimental evidence for such thermally-induced slip ratcheting is first provided in this work. It is implemented with an acryl sheet placed on an inclined wood with a mild angle; it is found that the temperature fluctuation of the acryl sheet causes the sheet to slide down gradually without any additional loading. The numerical model is then attempted to emulate the major findings of the experiments. From the simulation work, the location of a neutral point is found when the acryl plate is heated, and another neutral point is observed when cooled down. The shift of the neutral point appears to be a major reason for the unrecovered slip after a temperature increase and decrease cycle. Finally, a parametric study using the numerical model is carried out to examine which parameters play a major role in the development of residual slips.

Keywords: slip ratcheting; slip accumulation; temperature-induced displacement; repetitive temperature cycle; experimental study; numerical simulation

1. Introduction

Temperature fluctuation can cause various structural integrity problems at several different scales. Extreme heat can alter material properties by rearranging molecular structures, but even less severe temperature change can cause thermal cracking or buckling, as the material tends to expand and contract. Those temperature effects are relatively well-studied, but recently, some other cases were reported, which indicate moderately mild temperature change still could induce structural failure of the system—a slip accumulation (or allegedly “slip ratcheting”) over the interface between dissimilar materials accompanied with gravity. Examples of cyclic temperature and the corresponding displacement buildup of geotechnical systems are found in a variety of geotechnical problems, such as movements of natural rock slopes [1–3], exposed geosynthetic liners [4], pavement layers [5], and geothermal energy piles [6,7].

There are several common points in all these examples. First, a range of temperature change is not severe, so that the original material characteristics do not depreciate. Second, the interface slip corresponding to one temperature cycle is minor but continuously progresses as the number of cycles grows. Third, the whole system is equilibrated and stable before the temperature change, which means that an object on a slope has sufficiently large friction against the sliding. These points say temperature-caused interface slip accumulation can happen in any condition as long as two substances bear relatively different
thermal expansion coefficients under continuous temperature changes. It also leads to the point that the traditional sliding stability analysis (i.e., \( \mu > \tan \beta \), where \( \mu \) is a frictional coefficient and \( \beta \) is slope angle) may not be good enough to assess the long-term effect, especially under temperature fluctuation condition.

Unfortunately, there are not much reported observations of such slip ratcheting in many disciplines that can be used for in-depth follow-up study. Thermally-induced slip accumulation was first introduced for glacier slide by [8] and then a similar idea was later improved very recently by [5] for a pulsatile motion of pavement on the slope. On the other hand, geomembrane placed on construction slope also has been observed to experience thermal expansion and contraction (e.g., [9,10]); and Ref. [4] performed a lab test to see a geomembrane slippage over a slope. Ref. [2] attested that a slip accumulation indeed occurred in a field condition based on a field observation regarding the irreversible slip of a granite rock slab movement and estimated the future slippage with a numerical study.

All of these studies, however, use slightly different terminologies, ranging from “pulsatile motion” [5], “crawling theory” [11], “insolation creep” [5], to “displacement ratcheting” [12], which discloses there has not been sufficient study carried out to see the fundamental mechanism of “slip ratcheting” features. There is a clear need for future theoretical, numerical, and experimental work to extend their simple but robust approaches. Suggested future work includes more precise theoretical solutions, more realistic numerical simulations, carefully planned experimental investigations, and automated monitoring of displacements and temperatures of rock blocks at fields [2,5].

Most recently, [13] also suggested experimental evidence and a numerical algorithm on the thermal ratcheting problem. However, we still lack a fundamental understanding of the phenomena itself, and how it is affected by several influential parameters. In this regard, this study attempts to provide controlled experimental evidence and a numerical simulation approach for the study of thermally-induced displacement ratcheting. The produced work from this study helps reveal the fundamental features of the displacement ratcheting at an interface that can be expanded to the sustainable design of geostructures, such as geothermal energy piles, buried pipelines, exposed geosynthetic liners, and pavement layers, as well as the reliable prediction of the movement of natural rock slopes.

2. Experimental Observation

Experimental demonstration of the slip ratcheting is an essential part of this study as there are no sufficient studies in the literature, especially in a controlled condition. The experiment outcome obtained here can be utilized for both the evidence of slip ratcheting and the validation of the numerical simulation later. In this experiment, the material placed on the slope will undergo a number of heating–cooling cycles, and it is expected to continuously slide down with the number of cycles, that is, the slip ratcheting.

2.1. Slope Test

An overall test setup is shown in Figure 1a: an acryl plate sits on an inclined wood slope with an inclination angle of \( \beta \), and a heating pad is attached on the top of the acryl plate (Figure 1b). The inclination angle was selected to be \( \beta = 5° \) and 10°, so that the acryl plate does not slide down by gravity only—the critical inclination angle is around 15° (see Table 1). The acryl and wood materials are chosen to have a significant difference between thermal expansion coefficients of two materials (i.e., coefficients of linear thermal expansion are \( \sim 7 \times 10^{-5}K^{-1} \) for acryl vs. \( \sim 5 \times 10^{-6}K^{-1} \) for wood) and to minimize buckling or wrinkling effect when stretched. The dimension of the acryl plate is 12.7 cm \( \times \) 7.6 cm \( \times \) 0.25 cm (length \( \times \) width \( \times \) thickness). Other thermo-elastic properties of the acryl are summarized in Table 1. The electric heating pad, attached on the top of the acryl plate, is connected to a power supply and a switch that turns on-and-off for a designated time interval.
Figure 1. Experimental study of the thermally induced slip ratcheting. (a) Picture of the overall experimental setup, (b) schematic of the test design, (c) temperature fluctuation of the heating pad using a power supply and on-and-off switch, which results in the amplitudes of about 23 °C and 31 °C for 5 V and 6 V applied, respectively, and (d) an example of the slip ratcheting captured by the camera.
Table 1. List of thermoelastic properties of the acryl and the acryl-wood interface.

| Properties                           | Values               |
|--------------------------------------|----------------------|
| Young’s modulus of acryl, $E^*$      | 3.1 GPa              |
| Poisson ratio of acryl, $\nu^*$      | 0.37                 |
| Density of acryl, $\rho^*$           | 1.19 g/cm$^3$        |
| Linear thermal expansion coefficient of acryl, $\alpha^*$ | $7 \times 10^{-5}$ K$^{-1}$ |
| Linear thermal expansion coefficient of wood, $\alpha^*$ | $5 \times 10^{-6}$ K$^{-1}$ |
| Friction coefficient at acryl-wood interface, $\mu^{**}$ | 0.271 |
| Elastic limit at acryl-wood interface, $\delta^{**}$ | 0.01 mm |

* adopted from www.matweb.com (material property data webpage). ** determined by conducting direct shear tests in this study.

For the experimental demonstration, we applied the voltage of the power supply as 5 V and 6 V with the on-and-off time interval of the power supply as 10 min for the total experiment time of 12 h (i.e., total 36 heating–cooling cycles) (Figure 1c). Ten minutes of the heating–cooling duration is found sufficiently long to attain the consistent temperature at the acryl plate. During the test, the movement of the acryl plate was monitored using time-lapse photography (photo interval of 15 s) (Figure 1d). With the described test conditions (i.e., 5 V and 6 V of power supply for heating and 5° and 10° of the inclination angles), a total of 4 different cases are examined, and each case is performed twice for reproducibility. The amplitudes of temperature fluctuation are observed to be about 23 °C and 31 °C for 5 V and 6 V of applied powers, respectively (starting temperature is about 29 °C) (Figure 1c). There is no additional external force applied other than the temperature fluctuation during the tests. The accumulated slip is measured from the analysis of captured images of the acryl plate by the time-lapse camera, assuming the underlying wood slope is neither deforming nor moving.

For all conditions of the experiments, it is observed the slip values of the acryl plate over the wood slope are continuously growing. The amounts of slip are different, but they all linearly increase as the temperature fluctuation cycle continues. In general, the amount of accumulated slip becomes greater with a higher amplitude of temperature change and a larger inclination angle. The accumulated slip magnitudes are ranging from 1.075 mm ($\Delta T = 23 ^\circ C$ in $\beta = 5^\circ$ slope) to 2.910 mm ($\Delta T = 31 ^\circ C$ in $\beta = 10^\circ$ slope) after the 36 cycles. There are minor discrepancies in the results from the same experimental condition (i.e., same $\Delta T$ and $\beta$), but the overall tendency of the test results is consistent. As the slip increase is observed to be linear, the slip values after extended cycles can also be predicted via extrapolation of the first 20 cycles or so. In summary, the experimental results help to ascertain the ratcheting behavior of the slip growth and imply that the amount of slip will never be reduced down later (Figure 2).
2.2. Direct Shear Test

In parallel to the slope tests, direct shear tests (equipment: DigiShear™ by GeoTac) are conducted to identify the fundamental behavior of interfacial shear between the acryl plate and the wood slope and, thus, to understand the mechanism of the thermally-induced slip ratcheting more in-depth. The direct shear-type test is one of the popular geotechnical test methods for the evaluation of shear strength at the interface of materials in circular-upper and lower shear boxes (ASTM D3080 [14]). For this study, the same wood material is housed in the lower shear box, and the acryl is housed in the upper shear box (outer diameter: 63.5 mm). Once the two materials are in each shear box and are in contact, the normal stress is applied by the vertical actuator. A series of direct shear tests were performed under the various range of normal stresses, from 2.5 to 200 kPa, to evaluate the shear strength parameters. Note that the actual magnitude of the normal stress imposed on the acryl plate during the slope test is very small, about 29 Pa, only by the self-weight of the acryl plate. During the test, the acryl plate is horizontally pushed by the other actuator with the shear rate at 0.05 mm/min under the constant normal stress condition. The horizontal displacement of the shear box and the applied horizontal force are monitored during the test for analyzing the shear strength parameters at the acryl-wood interface. When the shear stress reaches the maximum value and then remains constant, the test is terminated.

Shear strength at the interface can be defined by a set of shear strength parameters—the coefficient of friction (µ) and the elastic limit (δ) of interface shear displacement (Figure 3). As shown in the plot of shear stress vs. displacement relationship, the interface shear behavior can be approximated with an elasto-perfectly-plastic constitutive model. The coefficient of friction (µ) remains practically constant over the entire range of the normal stress (Figure 4a), but the elastic limit (δ) is observed to be highly dependent on the normal stress (Figure 4b). The elastic limit for the condition of the slope test in this study is determined to be about ~0.01 mm based on the extrapolation of the observed elastic limits to the actual normal stress of ~29 Pa. The interface strength parameters are also summarized in Table 1.

![Figure 2](image_url)
Figure 3. Results of the direct shear test at the acryl-wood interface; (a) normalized shear stress versus shear displacement from the multiple direct shear tests under the various range of normal stresses (results shown here are for 10 kPa of normal stress as an example), and (b) conceptual idealization of the direct shear test result.
Figure 4. Results of the direct shear test at the acryl-wood interface; (a) determination of the frictional coefficient ($\mu$), and (b) elastic limits of the shear displacement ($\delta$) under various normal stresses and their regression fitting.

3. Numerical Study—Comparison with Experiment

Experiments reveal that the acryl plate gradually slides down (i.e., slip accumulation) only with the temperature variations. Even though the simple experiment can demonstrate the actual occurrence of slip ratcheting even under mild temperature changes, it is still not clear how the slip between two materials continuously grows and how much amount of the slip can be estimated after a large number of cycles. Moreover, there is a practical limitation of the number of temperature cycles that can be applied during the experimental study (e.g., the presented experimental work takes 12 h to monitor a gradual slip ratcheting over 36 cycles). In this respect, numerical analysis or analytical approach that can reproduce the described experimental results would be a great alternative, which will enable us to explore a much larger number of cycles.

The finite element model is constructed accordingly in the plane strain condition using Abaqus (Figure 5a). Note that a comparison between the two-dimensional plane strain and three-dimensional simulations is discussed in a later section. The acryl and wood in the simulation model are set as linear elastic materials with the representative mechanical
and thermal properties listed in Table 1. The interface is treated as linear elastic-perfectly plastic using the Coulomb frictional model. The coefficient of friction (μ) and the elastic slip (δ) are applied to the interface of those two materials. The wood is assumed not to deform against gravity nor temperature fluctuations, thus fully fixed in all directions, whereas the acryl plate as a sliding slab is not constrained at all. Similar to the experiment, the acryl plate is placed on the wood slope inclined at an angle of β, and only a gravitational acceleration is applied. Then, the temperature of the acryl plate is increased by ΔT and then decreased by the same temperature change (ΔT). The combination of temperature increase and decrease of the acryl plate is deemed one cycle of temperature fluctuation, and up to 50 temperature cycles are applied to the acryl plate during the numerical simulation. Similar to the experimental conditions, two cases of temperature changes (ΔT = 23 °C and 31 °C) and two cases of the inclination angles (β = 5° and 10°) are considered in the simulations for comparison with the experimental outcomes. The slip accumulation is monitored at the front end of the acryl plate (Figure 5a). Moreover, the stress values, along with the slip, are to be presented in the next section (following the definitions in Figure 5b). That is, σ_xx is the normal stress acting parallel to the slope surface, σ_yy is the normal stress acting perpendicular to the slope surface, and τ_xy is the shear stress between the acryl and the wood. All of these stress values are monitored at the base of the acryl. The positive normal stresses represent tensile values as per traditional mechanics and the negatives are for compressive ones. The positive shear stress denotes downward shear stress on the acryl side, which is the same as the one shown in Figure 5b.

![Figure 5](image)

**Figure 5.** (a) Conceptual schematic of the numerical model and (b) definitions of the stress values around the acryl plate.

Here are several simplifications made for the numerical works. First, material strength degradation with repetitive/cyclic thermal loading is not considered here. That
is, the interface strength between the acryl and wood assumed to have the same magnitude throughout the temperature cycles indefinitely. Moreover, although temperature increases at gradually decreasing rates during the experiments (blue squares in Figure 6a), it changes linearly in the simulation conditions (red dotted line in Figure 6a). Moreover, in the experiments, the acryl is heated from the top where the heating pad is attached, which might cause a minor temperature gradient inside the acryl; but the uniform temperature increase of the entire acryl plate is applied in the simulation. Finally, the acryl sliding is, rather, a three-dimensional feature, but the model described above uses a two-dimensional plane-strain condition. All simplifications made here are discussed further in the discussion section.

Figure 6. Comparison of the experiment and the simulation results with $\Delta T = 23 \, ^\circ C$ in $\beta = 5^\circ$ slope. (a) Temperature cycles during the actual experiments and the numerical simulations, and (b) slip accumulation of the acryl vs. temperature cycles.

For a better representation of the numerical result, the “residual values” of the slips (solid red line in Figure 6b) are primarily examined here instead of the entire trace of the
fluctuating slips (dotted red line in Figure 6b) with the temperature fluctuation. The “residual values” are the slip magnitudes after the temperature of the plate (ΔT) drops back to its initial temperature. In this way, the numerical result can be presented as simple straight lines instead of zigzag lines.

Comparisons of the experimental outcomes and the numerical results are summarized in Figure 7. The accumulated slip values after 20 cycles range from 1.245 mm (ΔT = 23 °C in β = 5° slope) to 3.485 mm (ΔT = 31 °C in β = 10° slope). These are somewhat close to that of the experiments ranging from 1.075 mm (ΔT = 23 °C in β = 5° slope) to 2.910 mm (ΔT = 31 °C in β = 10° slope). Apparently, there are certain discrepancies in the magnitudes of the accumulated slips. Nonetheless, the experimental outcomes and the numerical results can be regarded to be reasonably in good agreement in the aspect that the slip values all consistently and linearly increase, and the errors between the experiment and the simulation results are comparable to those between two experimental tests at the same condition.

Figure 7. Comparison of experiments and simulations—solid lines are the residual traces of numerical results and all the discrete markers are the experimental results.

**Numerical Study—Slip Behavior**

Upon the verification of the numerical model used for the thermally induced slip ratcheting in the previous section, the model now can be used to examine further how the interface strengths are mobilized during the slip ratcheting. We particularly focus on stress components and slip values at the interface in this section. The aim is to offer a better understanding of the behavior of the interface and the slip accumulation during temperature fluctuation. The coordinates for the stress components are shown in Figure 5b; the axis parallel to the slope is x-axis, and the one perpendicular is y-axis.

First, the distributions of normal stress in a direction parallel to the slope surface (σ_{xx}) on the acryl plate are shown in Figure 8. Normal stress with gravitational loading only is presented as a dotted-orange line (Figure 8), which magnitude is much smaller than that when any temperature changes are imposed. The distribution of normal stress with gravity appears nearly uniform, and the magnitude is around −4.2 Pa. With a temperature increase (labeled as “heating”), the distribution of normal stress (σ_{xx}) becomes negative (compressive), non-uniform, and concave-up with approximately −175 Pa of the peak at around 46 mm from the left end and nearly 0 Pa at both left and right ends of the acryl plate (a red line in Figure 8a). It implies that, when the acryl is heated, the entire acryl plate is under compressive stresses, caused by the constraint of the frictional resistance
between the acryl and the wood, namely, interface shear strength against thermal expansion behavior.

Once the temperature of the acryl drops back to the initial value (labeled as “cooling”), the normal stress ($\sigma_{nx}$) becomes positive (tensile) and its distribution in the plate is concave-down with the peak of $\sim$166 Pa around 81 mm from the left end of the acryl plate (a blue line in Figure 8a). In contrast to the heating cycle, the entire acryl plate is under tensile stresses with the temperature drop, and this is because the shrinkage of the acryl plate is obstructed by the interface shear stress. It is also observed that the distribution shapes and the stress magnitudes do not change as the temperature cycle continues. For instance, the distributions at the 50th cycle of temperature fluctuation are essentially the same as those of the first cycle (Figure 8b; the distributions at the first and 50th cycles are completely overlapped). With such a constant distribution of normal stresses, we can postulate that the locations of the maximum and the minimum normal stresses (i.e.,
81 mm and 46 mm from the left end, respectively) are approximately the “neutral points”. This will be discussed further in the next paragraph.

The distributions of normal stress in a direction perpendicular to the slope surface (σ_{yy}) at the base of the acryl plate is shown in Figure 9. Similar to σ_{xx} in Figure 8, the distribution shapes and the stress magnitudes of σ_{yy} also do not change during the 50 cycles of heating–cooling. The magnitude of σ_{yy} with gravitation loading only also more or less the same as those with temperature increase or drop, which is approximately 29 Pa, the value calculated in Section 2.2. There are small disturbances observed when the acryl is heated and cooled down; the amplitudes are up to 2 Pa, which is much smaller than the base value (29 Pa). The locations of the disturbances of σ_{yy} coincide with the location of the peak σ_{xx} values, (i.e., 81 mm and 46 mm from the left end, respectively).

![Figure 9](image.png)

**Figure 9.** Distributions of normal stress (σ_{yy}) on the acryl plate. The presented results are based on ΔT = 23 °C in β = 5° slope with the parameters in Table 1. (a) and (b) are the same as in Figure 8.

The distributions of interface shear stress (τ_{xy}) at the acryl-wood interface are presented in Figure 10. Note that shear stress is positive for the downslope direction and negative for the upslope at the lower surface of the acryl plate. Shear stress only with the
gravitational loading is also plotted in Figure 10 (a dotted orange line), which appears nearly uniform and small in magnitude (~2.5 Pa). With a temperature increase ("heating"), the shape of interface shear stress distribution is similar to a step function with a slanted jump from the minimum to the maximum (a dashed line in Figure 10a). The maximum and minimum values of shear stresses are nearly the same with the different signs, which implies that the interface shear stress reached its shear strength of \( \tau_f = 7.879 \text{ Pa} \) (note that \( \tau_f = \mu \rho gh \cos \beta = 0.271 \times 1.19 \frac{\text{m}}{\text{cm}^3} \times \frac{9.81 \text{m}}{\text{s}^2} \times 0.25 \text{ cm} \times \cos 5^\circ = 7.879 \text{ Pa} \)). Therefore, over the interval of 0 mm and 30 mm (from the left end, hereafter), the interface shear stress is approximately constant of \(-7.879 \text{ Pa}\), and over the interval of 51 mm to the right end, it is constant 7.879 Pa. Between 30 mm and 51 mm, the shear stress monotonically increases with zero at around 44 mm. Therefore, it can be inferred that a part of the acryl plate from the left end to 44 mm deforms upwards while the remaining part from 44 mm to the right end deforms downwards. Thus, the location of 44 mm can be considered as the "neutral point" when the acryl plate is heated, which is very close to 46 mm (determined from the normal stress distribution). Therefore, the estimate of 44 mm (determined from the shear stress distribution) is deemed as a more accurate one.

![Figure 10](image_url)

**Figure 10.** Distributions of interface shear stress \( (\tau_{xy}) \) at the acryl-wood interface. The presented results are based on \( \Delta T = 23 \, ^\circ\text{C} \) in \( \beta = 5^\circ \) slope with the parameters in Table 1. (a) and (b) are the same as in Figure 8.
With the temperature drop ("cooling"), the shape of interface shear stress distribution is flipped over (a solid line in Figure 10b) from that of the heating cycle, but with the different intervals for the maximum and minimum shear stresses. The interface shear stress is almost constant of 7.879 Pa over the interval of 0 mm and 77 mm, and it is again constant at −7.879 Pa over the interval of 98 mm to the right end. Between 77 mm and 98 mm, the shear stress decreases monotonically with zero at around 83 mm. Similar to the heating cycle, the location of 83 mm can be considered as the “neutral point” when the acryl plate is cooled down (81 mm from the normal stress distribution). Moreover, like the normal stress distribution, the distribution of interface shear stress remains the same during the 50th temperature cycles, which implies the stress conditions will not change hereafter.

The distribution of the interface slips at the acryl-wood interface is described in Figure 11. Positive values of the slip denote the downhill direction, whereas negative ones for the uphill movement. Slip by the gravitational loading only is negligible, as shown in Figure 11a (a dotted line; approximately 3.23 μm). When the temperature is increased, the slip distribution at the interface is linear, from −0.070 mm to 0.13 mm (from the left end to the right, a dashed line in Figure 11a). The location of zero slip appears to be approximately 44 mm, which coincides with the neutral point identified from the interface shear stress distribution (Figure 10). When the acryl plate is cooled back, the slip distribution is flipped over from 0.124 mm to −0.080 mm (from the left end to the right, a dot-dash line in Figure 11a), which shows another neutral point at 77 mm. The overall distribution of the slip after the combined heating–cooling cycle is approximately constant at 0.074 mm (a blue solid line in Figure 11a), which is fundamentally an irrecoverable, residual slip that is also shown in Figures 6b and 7.
There is a major difference found between the stress distributions (i.e., normal and shear) and the slip distribution; the slip distribution has an increasing magnitude with the repetition of the temperature cycle, whereas the stress distribution does not. As noted earlier, the same stress distribution shape during the temperature cycles implies that the locations of the neutral points are the same. The irrecoverable slip occurs even from the first heating–cooling cycle, which implies that the slip will continue to accumulate as the temperature cycle repeats. Moreover, the magnitude of the irrecoverable slip at each heating–cooling cycle must be the same, given that the stress values are identical during all the cycles. Therefore, the irrecoverable slip will continuously grow with the temperature cycles, and it should be linearly growing. For instance, the irrecoverable slip is 0.003 mm with the gravity, 0.074 mm at the first cycle, 0.646 mm at the 10th cycle, and then
3.213 mm at the 50th cycle (solid lines in Figure 11b,c), which is approximately 0.064 mm/cycle.

Similar features are also found in the different case with the higher temperature amplitude and slope angle, $\Delta T = 31^\circ \text{C}$ in $\beta = 10^\circ$ slope (Figure 12 through Figures 13 and 14). The overall patterns of the normal stress ($\sigma_{zz}$), interface shear stress ($\tau_{xy}$), and slip at the acryl-wood interface are found similar. However, the magnitudes of the stresses and the slips along with the neutral point positions are quite different from those from the previous condition ($\Delta T = 23^\circ \text{C}$ in $\beta = 5^\circ$ slope). For example, the minimum normal stress is about $-110.7$ Pa around 29 mm (from the left end hereafter) when heated, and the maximum value comes at about 101.3 Pa around 98 mm when cooled down (Figure 12). Zero interface shear stress is observed at around 23 mm and 104 mm when heated and cooled down, respectively, and the neutral points are identified as those locations accordingly. The intervals of the shear stress transition are between 8 mm and 32 mm and between 95 mm and 119 mm when heated and cooled down, respectively (Figure 13). Moreover, after the first heating–cooling cycle, the residual slip is 0.358 mm (0.184 mm slip with gravity), and it accumulates to 1.744 mm after 10 cycles, and to 8.717 mm after 50 cycles, which is approximately 0.171 mm/cycle (Figure 14). Please be noted that the described features in the distributions of normal and stress forces and the slip values are also presented in [13] to some extent.
**Figure 12.** Distributions of normal stress ($\sigma_{xx}$) on the acryl plate. The presented results are based on $\Delta T = 31 \, ^\circ C$ in $\beta = 10^\circ$ slope with the parameters in Table 1. (a) and (b) are the same as in Figure 8.

![Graph of normal stress](image)

**Figure 13.** Distributions of interface shear stress ($\tau_{xy}$) at the acryl-wood interface. The presented results are based on $\Delta T = 31 \, ^\circ C$ in $\beta = 10^\circ$ slope with the parameters in Table 1. (a) and (b) are the same as in Figure 8.

![Graph of interface shear stress](image)
Figure 14. Distributions of the interface slip. The presented results are based on $\Delta T = 31^\circ \text{C}$ in $\beta = 10^\circ$ slope with the parameters in Table 1. (a), (b), and (c) are the same as in Figure 11.
As shown in those two cases of simulations, the magnitude of a residual slip is affected by the location of the neutral points. It helps to consider an extreme case where the neutral point is exactly at the middle of the acryl plate: that is, when the acryl is placed on a flat surface ($\beta = 0^\circ$), then the neutral point is always at the half of the plate during both heating and cooling conditions. Intuitively, no irrecoverable slip is expected in this case. Therefore, the flip of the neutral point about the center of the plate during the heating-and-cooling cycles is believed to be a primary reason for such a residual slip. Moreover, the irrecoverable slip would increase as the distance from the neutral point to the middle of the plate lengthens.

Lastly, Figure 15 describes the stress–slip relations during the repetitive heating–cooling cycles. The magnitude of the interface slip continuously grows while the interface shear stress alternates only within the same maximum and minimum values. That is, with the same temperature fluctuations, the slip ratcheting would gradually occur and continue to accumulate during the temperature cycles.

![Graph](attachment:graph.png)

**Figure 15.** The slip build-up during the 50 temperature cycles. The presented results are based on the parameters in Table 1 with (a) $\Delta T = 23^\circ C$ in $\beta = 5^\circ$ slope and (b) $\Delta T = 31^\circ C$ in $\beta = 10^\circ$ slope.
4. Numerical Study—Parametric Study

As revealed in the previous section, all these results—residual displacement, normal stresses, neutral point, and interface shear stress—are unique outcomes of each input parameter set. Therefore, the impact of individual input parameters on the presented model needs to be identified more; in this regard, we applied the seven different parameters—temperature amplitude ($\Delta T$), elastic limit at the interface ($\delta$), linear coefficient of thermal expansion ($a$), slope angle ($\beta$), coefficient of friction ($\mu$), density of the sliding material ($\rho$), and Young's modulus ($E$)—from the base case. The base case is the set of parameters in Table 1 with $\Delta T = 23^\circ C$ and $\beta = 5^\circ$ slope ($\delta = 0.01$ mm, $a = 7 \times 10^{-5}$ K$^{-1}$, $\mu = 0.271$, $\rho = 1.19$ g/cm$^3$, and $E = 3.1$ GPa). In this section, each one of these base case parameters is changed independently, and the corresponding results are compared. For example, three different temperature amplitudes, $\Delta T = 23^\circ C$, $31^\circ C$, and $39^\circ C$, are examined as shown in Figure 16a. The base case is marked with a thick solid line, and the other two are drawn with thin solid lines. Experimental test results observed in Figure 2 are also presented as a series of markers for comparisons.
Figure 16. A parametric study with different inputs of temperature amplitude, elastic limit of the interface slip, and thermal expansion coefficient in (a), (b), and (c). The base case is set to $\Delta T = 23$ °C and $\beta = 5°$ slope with the parameters in Table 1. Two experimental test results (1 and 2) for the base case are from Figure 2. A parametric study with different inputs of slope angle, friction coefficient, and acryl density in (d), (e), and (f). The base case is set to $\Delta T = 23$ °C and $\beta = 5°$ slope with the parameters in Table 1. A parametric study with different inputs of Young’s modulus in (g). The base case is set to $\Delta T = 23$ °C and $\beta = 5°$ slope with the parameters in Table 1.

As a result of simulations, the magnitude of accumulated slip increases with the higher values of $\Delta T$, $\alpha$, and $\beta$, and the lower value of $\mu$. On the other hand, other parameters, including $\delta$, $\rho$, and $E$, make a lesser impact or insignificant influence on the accumulated slip values. This observation agrees well with the landslide stability formula from geotechnical engineering [15], where the factor of safety for cohesionless soils is independent of the soil density.

The parametric study also shows the possible range of the residual slip accumulation after 50 temperature cycles. It can be inferred that the magnitude can be as small as $<1\text{ mm}$ with a certain combination of the input parameters, but on the other hand, the magnitude could be possibly larger than $10\text{ mm}$ in 50 cycles. Understanding that the slip value will only increase and never decrease, with a much larger number of temperature
cycles, the slip can be piled up to the level with which the structural stability is critically hampered.

5. Discussion

As many computational works do, the presented model has some approximations implemented for the numerical study. Even though those approximations are not uncommon in many numerical studies and geotechnical engineering disciplines, the impact of those approximations is investigated here.

In this study, a two-dimensional (2D) plane strain numerical model is employed instead of a three-dimensional (3D) one, which would emulate the experimental condition better. In Figure 17, there is a certain difference between the 2D and 3D analyses, 3.213 mm and 2.522 mm after 50 temperature cycles, respectively. The discrepancy between these two approaches (approximately 21%) is not significantly large, considering the complexity of the slip ratcheting conditions. In fact, although running a 2D numerical model is neither dramatically faster nor easier, it is very typical to simplify a landslide problem into the 2D plane-strain condition in the discipline of geotechnical engineering ([15]). Furthermore, understanding the 2D model will surely be helpful to appreciate the 3D model. Particularly in this study, the 2D analysis has a great advantage over the 3D analysis because we aim to develop a theoretical approach for solving the slip ratcheting problem analytically in the following study.

Another approximation made in the numerical model is how the heating is applied to the acryl plate. In the experiments, the top of the acryl plate is heated by the heating pad attached to it. Then, the entire acryl plate is heated by the heat conduction, resulting in a temperature gradient in the transverse direction. On the other hand, the temperature of the entire acryl plate is increased at the same rate in the numerical model (that is, no temperature gradient). Hence, simulations in which a heat source is imposed at the top surface would rather reflect heat flux, and thus the transient temperature change in the acryl better. Simulations with such a setting were also conducted, and we compared the results in both 2D and 3D conditions; temperature inputs at the bottom of the acryl plate over the heating–cooling cycle are described in Figure 18a. There are no significant differences between the cases of experimentally measured one, simulation with constant temperature change, and simulation with transient temperature change. The residual slip, on the other hand, show much less difference. The slip values are 0.074 mm and 0.060 mm from the 2D and 3D analyses with the constant temperature change and 0.077 mm and
0.071 mm for the 2D and 3D analyses with the transient temperature change. The direct experimental value is not available but can be estimated as 0.067 mm based on the trend line (a dotted blue line) of experimental observation.

Figure 18. Effect of the transient heating condition on the residual slip. (a) Temperature change during the first heating–cooling cycle and (b) slip change.

6. Conclusions

Experimental evidence of the thermally-induced slip ratcheting is provided in this study, using an acryl sheet placed on a mildly-inclined wood slope. As a result of temperature increase and decrease of the acryl sheet, without any further loading, the sheet is observed to slide down gradually and continually. This is a consistent result with the other experiment settings, i.e., different temperature amplitudes and inclination angles.

The numerical model and simulation are also attempted to reproduce the major findings of the experiments. From the simulation work, it is found that there exists a neutral point in the acryl plate, and its location differs between the heating and cooling cycle of the plate. The shift of the neutral point appears to be the major reason for the residual slip.
after the temperature increase and decrease cycle because all the stresses are incurred repeatedly the same between the identical upper and lower limits. Although the magnitude of the residual slip is insignificant with one cycle, it continues to accumulate with a large number of cycles and could be sufficiently large to affect the overall stability.

The parametric study with the presented numerical model is also carried out to identify which input parameters play a major role in magnifying the residual slip values. It turns out that the accumulated slip values amplify with the increase of temperature amplitude ($\Delta T$), the coefficient of linear thermal expansion ($a$), and slope angle ($\beta$), and with the decrease in the coefficient of friction ($\mu$). However, the elastic limit at the interface ($\beta$), the density of the sliding material ($\rho$), and Young’s modulus ($E$) make a lesser impact or insignificant changes on the accumulated slip values.

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**Reference**

1. Bakun-Mazor, D.; Hatzor, Y.H.; Glaser, S.D.; Santamarina, J.C. Thermally vs. seismically induced block displacements in Masada rock slopes. *Int. J. Rock Mech. Min. Sci.* 2013, 61, 196–211.
2. Kim, S.; Druszkowski, E.; Zhang, J.; Kim, S. Numerical study on thermally-induced displacement ratcheting of a thin rock slab. In Geo-Congress 2019: Geotechnical Materials, Modeling, and Testing; American Society of Civil Engineers: Reston, VA, USA, 2019; pp. 506–513, doi:10.1061/9780784482124.051.
3. Meier, J.; Bock, H. Stability of a block resting on an inclined plane—A classical problem revisited. *Int. J. Rock Mech. Min. Sci.* 2014, 70, 407–417.
4. Pastén, C.; Santamarina, J.C. Experimental and numerical modeling of thermally-induced ratcheting displacement of geomembranes on slopes. *Geosynth. Int.* 2014, 21, 334–341.
5. Croll, J.G.A. Thermally induced pulsatile motion of solids. *Proc. R. Soc. A* 2009, 465, 791–807.
6. Murphy, K.D.; McCartney, J.S.; Henry, K.S. Evaluation of thermo-mechanical and thermal behavior of full-scale energy foundations. *Acta Geotech.* 2015, 10, 179–195.
7. Suryatriyastuti, M.E.; Mroueh, H.; Burlon, S. A load transfer approach for studying the cyclic behavior of thermos-active piles. *Comput. Geotech.* 2014, 55, 378–391.
8. Moseley, H. Descent of a solid body on an inclined plane when subject to alternations in temperature. *Proc. R. Soc.* 1855, vii, 333–342.
9. Rowe, R.K. Long-term performance of contaminant barrier systems. *Géotechnique* 2005, 55, 631–678.
10. Take, W.A.; Chappel, M.J.; Brachman, R.W.I.; Rowe, R.K. Quantifying geomembrane wrinkles using aerial photography and digital image processing. *Geosynth. Int.* 2007, 14, 219–227.
11. Uchida, E.; Azumi, R.; Norikane, Y. Light-induced crawling of crystals on a glass surface. *Nat. Commun.* 2015, 6, 7310.
12. Pastén, C.; Garcia, M.; Cortes, D.D. Physical and numerical modeling of the thermally induced wedging mechanism. *Geotech. Letters* 2015, 5, 186–190.
13. Pastén, C.; Castillo, E.; Chong, S.H. Thermo-mechanical ratcheting in soil-structure interfaces. *Acta Geotech.* 2019, doi:10.1007/s11440-019-00816-8.
14. ASTM D3080/D3080M-11, Standard Test Method for Direct Shear Test of Soils Under Consolidated Drained Conditions; ASTM International: West Conshohocken, PA, USA, 2011.

15. Duncan, J.M.; Wright, S.G.; Brandon, T.L. Soil Strength and Slope Stability, 2nd ed.; John Wiley & Sons, Inc.: Hoboken, NJ, USA, 2014; 317p.