Fermi surface of superconducting LaFePO determined from quantum oscillations

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We report extensive measurements of quantum oscillations in the normal state of the Fe-based superconductor LaFePO, \((T_c \sim 6 \text{ K})\) using low temperature torque magnetometry and transport in high static magnetic fields (45 T). We find that the Fermi surface is in broad agreement with the band-structure calculations with the quasiparticle mass enhanced by a factor \(\sim 2\). The quasi-two dimensional Fermi surface consist of nearly-nested electron and hole pockets, suggesting proximity to a spin/charge density wave instability.

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The recent discovery of superconductivity in ferrooxypnictides \cite{1,2}, has generated huge interest as another possible route towards achieving high \(T_c\) superconductivity. LaFePO was among the first Fe-based superconductor to be discovered and has a transition temperature of up to \(T_c \sim 7 \text{ K}\) \cite{1}. This compound is isostructural with LaFeAsO, which is non-superconducting and has a spin-density wave (SDW) ground state \cite{4}, but becomes a relatively high-\(T_c\) superconductor \((T_c \approx 25 \text{ K})\) when electron doped \cite{5}. By changing the rare-earth ion, \(T_c\) reaches 55 K in SmFeAsO\(_{1-x}\)F\(_x\) \cite{2}. Theoretical models suggest that the pairing mechanism in the Fe-based superconductors may be mediated by magnetic fluctuations due to the proximity to a SDW \cite{2,4,6}. Knowing the fine details of the Fermi surface topology, its tendency towards instabilities as well as the strength of the coupling of the quasiparticles to excitations is important for understanding the superconductivity.

Quantum oscillations provide a bulk probe of the electronic structure, giving detailed information about the Fermi surface (FS) topology and mass renormalization. To observe quantum oscillations samples must be extremely clean and the upper critical field must be low enough for the normal state to be accessed; LaFePO is a material which fulfills both these requirements. The tetragonal layered structure of LaFePO is made of alternating highly conductive FeP layers and poorly conducting LaO layers stacked along the \(c\) axis \cite{6}. Here we report extensive measurements of quantum oscillations in torque and transport data. We find that the Fermi surface of LaFePO is composed of quasi two-dimensional nearly-nested electron and hole pockets with moderate enhancement of the quasiparticle masses.

Single crystals of LaFePO, with dimensions up to \(0.2 \times 0.2 \times 0.04 \text{ mm}^3\), and residual resistance ratios \(\rho(300 \text{ K})/\rho(10 \text{ K})\) up to 85, were grown from a tin flux \cite{9}. Single crystal x-ray diffraction gives lattice parameters \(a = 3.941(2) \text{ Å}, c = 8.507(5) \text{ Å}\), and La/P positions \(z_{La} = 0.148901(19), z_{P} = 0.63477(10)\) in agreement with previous results \cite{1}. Torque measurements were performed with piezoresistive microcantilevers \cite{10} down to 0.3 K on different single crystals from the same batch \((T_c \approx 6 \text{ K})\); one in Bristol up to 18 T (sample B) and another crystal at the NHMFL, Tallahassee, up to 45 T (sample A). Interplane electrical transport has been measured on a third sample (sample C).

Figure 1a shows raw torque measurements versus magnetic field at low temperatures \((T = 0.3 \text{ K})\) at various angles \(\theta\) between the magnetic field direction and the \(c\) axis \cite{12}. At low fields we observe behavior typical of a bulk anisotropic type-II superconductor in the vortex state \cite{11}. The signal is reversible, indicating weak pinning of vortices. The upper critical field \((F_{c1})\) is strongly anisotropic, varying between \(\mu_0H_{c2} = 7.2 \text{ T}\) when the magnetic field is parallel to the \(ab\) plane and \(\mu_0H_{c2} = 0.68 \text{ T}\) when \(B||c\). For magnetic fields above \(\sim 9 \text{ T}\), we observe oscillations periodic in inverse field, which arise from the de Haas-van Alphen (dHvA) effect. The oscillatory signal is clearly visible by subtracting a monotonic background (a fifth-order polynomial) from the torque data \((\text{dHvA in Fig.1b})\) or transport data \((\text{Shubnikov-de Haas effect (SdH) in Fig.1c})\).

From the fast Fourier transform (FFT) spectra of the oscillatory data (Figs. 1d and 1e) we can identify the dHvA frequencies \(F\), which are related to the extremal cross-sectional areas \(A_k\) of the FS orbits via the Onsager relation, \(F = (\hbar/2\pi\epsilon)A_k\). From the evolution of these frequencies as the magnetic field is rotated from being along the \(c\) axis \((\theta = 0^\circ)\) towards the \(a\) axis \((\theta = 90^\circ)\), we can construct a detailed three dimensional picture of the shape and size of the Fermi surface. Four frequencies have significantly larger amplitudes than the others in both samples A and B as shown in Figs. 1d and 2a. We label \(\alpha_1\) and \(\alpha_2\) the two closely split frequencies at \(F \approx 1 \text{ kT}\) \((\Delta F \approx 35 \text{ T})\) and the two higher frequencies, \(\beta_1\) and \(\beta_2\). Besides these intense features (and their harmonics \cite{10}), in sample A (which was measured to
FIG. 1: (color online) a) Torque measurements on LaFePO measured at $T = 0.35$ K and in magnetic fields up to 18 T for different magnetic field directions. The arrows indicate the position of $H_{c2}$. b) Oscillatory part of the torque (dHvA) and c) resistance (SdH) in magnetic fields up to 45 T. d) Fourier transform spectra (field range 15-45 T) for two different magnetic field directions. e) The angle dependence of the Fourier transform spectra for the field range 10-18 T (sample B).

much higher fields) we see several other frequencies with smaller amplitudes; these are labeled $\gamma$, $\delta$, $\epsilon$ and have frequencies in the range 0.7–1.7 K T. An extremely weak signal, $\eta$, was observed only in sample B (measured up to 18 T) which we believe originates from a small misaligned crystallite $[12]$. The observed frequencies correspond to a fraction varying between 2.8% to 9% of the basal plane area of the Brillouin zone. They are significantly larger than those observed in the double-layer Fe-As compound, SrFe$_2$As$_2$ $[13]$, which is non-superconducting, and is likely to have a reconstructed Fermi surface at low temperatures due to a spin-density-wave ground state.

Figs. 1e and 2a show the angular dependence of the main frequencies and their amplitudes. For a purely two-dimensional cylindrical Fermi surface the dHvA frequency varies like $1/\cos \theta$ and deviations from this indicate the degree of warping for a quasi-two-dimensional cylinder. As shown in Fig. 2b, the orbits $\beta_1$ and $\beta_2$ both originate from sections of FS which have significant warping, but with opposite curvature (i.e., maximal and minimal areas respectively). The angle dependence of these orbits is well described by Yamaji’s analysis of simple cosine warping of a two-dimensional cylinder $[14]$, as is the large increase in the amplitude of the oscillations at $\theta \sim 45^\circ$, where the frequencies cross (see Fig. 1e). These observations indicate that $\beta_1$ and $\beta_2$ arise from the same FS sheet. For the $\alpha$ orbits the warping of the FS sheet is very small, but the almost identical amplitudes, effective masses (see below) and frequencies strongly suggests that these orbits arise from a single, weakly warped, FS sheet.

The effective mass of the quasiparticles on the various orbits were determined by fitting the temperature dependent amplitude of the oscillations to the conventional Lifshitz-Kosevich formula $[15]$, as shown in Fig. 2c. The obtained masses range between $1.7 m_e$ and $2.1 m_e$ and are listed in Table I ($m_e$ is the free electron mass).

We now compare our experimental observations with predictions of the density functional theory calculations of the electronic structure of LaFePO. Our calculations were made using the WIEN2K code with the experimental lattice parameters and atomic positions and including spin-orbit interactions $[16]$. The resulting band structure is in good agreement with that reported by Lebégue $[8]$. The density of states at the Fermi level are derived mainly from Fe and P bands suggesting that the carriers flow mainly in the 2D Fe-P layer. The Fermi surface
TABLE I: Effective masses ($m^*$) and frequencies from dHvA data for samples A and B. Calculated band masses ($m_b$) in LaFePO for shifted and unshifted bands. Orbits are labeled by band number and the location of their center.

| Branch (exp.) | $F (kT)$ | $m^*/m_e$ (Sample A) | $m^*/m_e$ (Sample B) | Orbit $(m_b/m_e)$ (calc.) | unshifted | shifted |
|---------------|----------|----------------------|----------------------|--------------------------|-----------|---------|
| $\alpha_1$   | 0.985(7) | 1.9(2)               | 1.8(1)               | 1Z                       | 1.0       | 1.9     |
| $\alpha_2$   | 1.025(7) | 1.9(2)               | 1.8(1)               | 2\Gamma                  | 0.9       | 0.7     |
| $\beta_1$    | 1.91(1)  | 1.7(2)               | 1.8(1)               | 2Z                       | 1.2       | 1.1     |
| $\beta_2$    | 2.41(1)  | 1.8(2)               | 1.9(1)               | 3\Gamma                  | 1.8       | 1.1     |
| $\gamma$     | 1.36(2)  | 1.8(3)               |                      | 3Z                       | 2.9       | 2.5     |
| $\epsilon$   | 0.73(2)  | 1.7(3)               |                      | 4M                       | 0.7       | 0.7     |
| $\epsilon'$  | 1.69(2)  | 2.1(3)               |                      | 4A                       | 0.9       | 0.9     |
| $\epsilon''$ |          |                      |                      | 5M                       | 0.8       | 0.7     |

FIG. 3: (color online) a) Calculated dHvA frequencies versus angle for unshifted bands compared to experimental data (shown in light blue) b) As in a) but for shifted bands (see text). c), d) Two-dimensional (110) cuts of the Fermi surface for unshifted and shifted bands, respectively. Solid black lines indicate the Brillouin zone. A possible inter-band nesting vector, $Q \approx [\pi, \pi, 0]$, between electron and hole bands is shown.

mainly comprises small, slightly warped tubular sections running along the $c$ direction. There are two hole cylinders centered on the Brillouin zone centre (Γ) and two electron cylinders centered on the zone corner (M) (see Fig. 3c-f). In addition, there is a small three-dimensional (3D) hole pocket centered on Z. The spin-orbit interaction makes small but significant changes to the Fermi surfaces; most notably it breaks the degeneracy of the bands crossing the Fermi level along the XM line such that the two cylindrical Fermi surfaces no longer touch and it also increases the separation of the elliptical hole pocket and the two cylindrical hole surfaces (Fig. 3c).

The frequencies of the extremal dHvA orbits obtained from the calculated band structure are compared with the experimental data in Fig. 3a. The calculation predicts that there should be 9 frequencies (two for each tube plus one for the 3D hole pocket) in the range $0.7-3$ kT (for $\theta \approx 0^\circ$), which is broadly similar to what is observed experimentally. In particular orbits $\alpha_1$ and $\alpha_2$ are very close to that of the smaller electron cylinder. The larger amplitude of these oscillations indicates that they both suffer significantly less damping than the other orbits (we estimate a mean free path of $\approx 1300 \, \text{Å}$ and $800 \, \text{Å}$ for $\alpha$ and $\beta$ orbits, respectively). This may be a natural consequence of the fact that both of these electron orbits originate from the same piece of Fermi surface in the larger unfolded Brillouin zone (corresponding to the Fe-sublattice [5]). Assuming the above assignment for the $\alpha$ and $\beta$ frequencies, the three remaining frequencies ($\gamma$, $\delta$, $\epsilon$) would then correspond to hole orbits, although their exact assignment is less clear. For these hole orbits the scattering is a factor $\sim 2$ larger than the electron orbits (Figs. 1d and 1e).

Performing small rigid shifts of the energies of the electron and hole bands improves the agreement with experiment. The two bands giving rise to the electron orbits $\alpha$ and $\beta$ are shifted by $-83$ meV and $-30$ meV, respectively and the hole bands by $+53$ meV (Fig. 3b). The band that gives rise to the 3D pocket (which we do not observe experimentally) influences significantly the degree of warping along the $c$-axis of the hole cylinders; if this band was absent we would have a better agreement between our data and calculations (Figs. 3a and 3b).

A two-dimensional cut in the ΓXM plane for our calculated unshifted and shifted Fermi surface (see Figs. 3e and 3f) shows that the electron pockets at the corner of the Brillouin zone (M) have almost similar shapes and sizes to the hole pockets at the centre of the zone (Γ). Nesting requires a perfect match between the size and the Fermi surface topology of the electron and hole pockets and this could stabilize a spin density wave (magnetic order) or charge density wave (structural order) with a wave vector $Q \approx [\pi, \pi, 0]$ [8, 18, 22]. LaFePO is non-magnetic but importantly our results suggest that size and the shape of the electron and hole pockets are indeed very similar (Figs. 3e and f) implying that LaFePO...
may be close to nesting and hence to a spin/charge density wave instability.

For an undoped LaFePO the volume of the electron and hole sheets should be equal (compensated metal) but shifting the bands (as described above) creates an imbalance of $\sim 0.03 \, \text{electrons per formula unit}$. A possible explanation for this imbalance can be related to a small amount of electron doping in our crystals due to oxygen non-stoichiometry ($\sim 1.5 \%$ oxygen deficiency which is below the resolution of our x-ray data).

The band structure calculation allows us to estimate the many-body (electron-phonon and electron-electron) enhancements of the quasiparticle masses over their band values. Table I shows the band masses for all the predicted orbits as calculated, and after application of band shifts. For the identified bands a moderate renormalisation is found, with $m^*/m_b = (1 + \lambda) \approx 2$. For the hole orbits the calculated frequencies do not correspond exactly to the experimental ones, however, as the band masses for most of the hole orbits are in the range $0.7 - 1.1 \, m_e$ and the measured $m^*$ values are $\approx 2m_e$, a similar level of enhancement is likely. Reported measurements of the electronic specific heat coefficient ($\gamma$) vary between 7-12 $\text{mJ/mol K}^2$ [8, 17, 18]. In 2D materials $\gamma$ can be estimated from the renormalised dHvA masses, summed over all of the observed FS sheets. Four quasi-2D FS sheets with an effective mass $\sim 2m_e$ would give $\gamma_{dHvA} \sim 6 \text{mJ/mol K}^2$, close to the lower end of the experimentally observed values, without including any contribution from a 3D pocket.

A recent ARPES study of LaFePO [9] showed an electron-like FS pocket centered at the M point and two hole sheets at the $\Gamma$ point. The electron sheet and the smaller hole orbit have areas close to the experimentally observed dHvA frequencies. When compared to band structure calculations, the bands found in the ARPES measurements are renormalized by a factor two, similar to the mass enhancements we have found. This suggests that the renormalization occurs over the whole band, rather than being localized to energies close to the Fermi level, as found in Sr$_2$RuO$_4$. [20] One of the hole pockets seen in ARPES is much larger ($> 12 \, \text{kT}$) than any dHvA frequencies observed here; its presence creates a significant charge imbalance of one electron per unit cell, suggesting that this feature is related to surface effects.

As in the other ferrooxypnictides, in LaFePO the band-structure is very sensitive to the position of the P atom [21, 22]. Considering the P atom in the position optimized (the ‘relaxed’ structure) results in hole orbits which are much too small to explain our data. Much larger band energy shifts are needed to bring it into approximate agreement and we find that the band structure calculated with the experimental P position provides a better description of the data.

In conclusion, we have found experimentally that the Fermi surface of the superconductor LaFePO, is in broad agreement with band structure calculations with a mass enhancement of about 2 due to many-body interactions. The difference in amplitudes of the dHvA signal between the hole and electron pockets is an indication of different scattering rates affecting these orbits. The near-perfect matching between the hole and the electron orbits that we observe, suggests that LaFePO may be close to a spin/charge density wave transition and that magnetic fluctuations are an important ingredient in the physics of the Fe-based superconductors.

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