Wide Twin Binaries are Extremely Eccentric: Evidence of Twin Binary Formation in Circumbinary Disks

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Abstract

The Gaia mission recently revealed an excess population of equal-mass “twin” wide binaries, with mass ratio \( q \gtrsim 0.95 \), extending to separations of at least 1000 au. The origin of this population is an enigma: Twin binaries are thought to form via correlated accretion in circumbinary disks, but the typical observed protostellar disks have radii of \( \sim 100 \) au, far smaller than the separations of the widest twins. Here, we infer the eccentricity distribution of wide twins from the distribution of their \( v-r \) angles, i.e., the angle between the components’ separation and relative velocity vectors. We find that wide twins must be on extremely eccentric orbits. For the excess-twin population at 400–1000 au, we infer a near-delta-function excess of high-eccentricity systems, with eccentricity \( 0.95 \lesssim e \lesssim 1 \). These high eccentricities for wide twins imply pericenter distances of order 10 au and suggest that their orbits were scattered via dynamical interactions in their birth environments, consistent with a scenario in which twins are born in circumbinary disks and subsequently widened. These results further establish twin wide binaries as a distinct population and imply that wide twins can be used as a probe of the dynamical history of stellar populations.

Unified Astronomy Thesaurus concepts: Binary stars (154); Wide binary stars (1801); Eccentricity (441); Circumstellar disks (235)

1. Introduction

Binary population demographics encode information about the star formation process and subsequent dynamical processing. One striking feature of the binary population is the existence of an excess population of equal-mass “twin” binaries with mass ratios \( 0.95 \lesssim q \lesssim 1 \), where \( q = M_2/M_1 \) and \( M_1 \) and \( M_2 \) are the masses of the primary and secondary. This twin excess is strongest at short periods and was long thought to exist only at orbital periods \( P_{\text{orb}} \lesssim 40 \) days (e.g., Lucy & Ricco 1979; Tokovinin 2000). However, studies of large samples of binaries have recently shown that an excess population exists even at very wide separations, extending beyond 1000 au for solar-type stars (e.g., Soderhjelm 2007; Moe & Di Stefano 2017; El-Badry et al. 2019).

The leading hypothesis for the origin of the twin excess is that twins form in circumbinary disks. In this scenario, the lower-mass star has a higher accretion rate from the circumbinary disk due to its wider orbit around the common center of mass or due to the dynamics of the accretion streams (Bate & Bonnell 1997; Farris et al. 2014; Young & Clarke 2015; Duffell et al. 2020), thus driving the mass ratio to unity. Torques from the disk may also shrink the binary orbit, potentially explaining why the amplitude of the twin excess is largest at close separations (Tokovinin & Moe 2020). However, this picture is still under debate. First, it is unclear whether the lower-mass star in a circumbinary disk will always have the higher accretion rate, with different codes making qualitatively different predictions (Bate & Bonnell 1997; Ochi et al. 2005) and the behavior may depend on gas temperature (Young et al. 2015; Young & Clarke 2015). Furthermore, how the interaction between the binary and the circumbinary disk affects a binary’s orbital evolution remains an open question (Artymowicz et al. 1991; Artymowicz & Lubow 1994; Pichardo et al. 2005; Shi et al. 2012; Miranda et al. 2017; Moody et al. 2019; Muñoz et al. 2019; Heath & Nixon 2020; Ragusa et al. 2020; Tiede et al. 2020; Dittmann & Ryan 2022). Thus, twin binaries provide a unique observational opportunity to study the effects of accretion from circumbinary disks.

The excess of twin binaries with separations \( \gtrsim 100 \) au is particularly puzzling (Soderhjelm 2007). Their existence out to \( >1000 \) au is now confirmed by Gaia and is not due to selection effects (El-Badry et al. 2019). Observed protoplanetary and circumbinary disks have typical radii of \( \sim 100 \) au (e.g., Andrews et al. 2018; Ansdell et al. 2018; Manara et al. 2019), and so wide twins cannot have formed in circumbinary disks at their current separations. Although the excess-twin population only contains a few percent of all binaries at these separations, the twin excess is manifest as a sharp, step-function-like jump in the mass-ratio distribution above \( q_{\text{win}} \sim 0.95 \) (El-Badry et al. 2019). Because \( q_{\text{win}} \) does not vary between close and wide binaries, it is natural to assume that wide twins form via the same process as close twins. One possible formation scenario is that wide twins formed at closer separations (10–100 au) within a circumbinary disk and were subsequently widened by dynamical interactions. However, the nature of this interaction and widening process is poorly understood.
If the twins’ formation involves dynamical widening either through gravitational interactions with other stars, or through recoils or kicks to one of the components, then highly eccentric orbits are expected for wide twins. Furthermore, binary eccentricities are a direct prediction from simulations of binary–circumbinary disk interaction (e.g., Artymowicz & Lubow 1994; Roedig et al. 2011; Muñoz et al. 2019; Dittmann & Ryan 2022). Therefore, the eccentricity of wide twin binaries is a critical connection between observational and theoretical work.

In this Letter, we investigate the eccentricities of wide twin binaries. The individual eccentricities of wide binaries are challenging to measure due to their long orbital periods (≥10^7 yr for binaries at >10^5 au), but the population eccentricity distribution can be statistically constrained by the distribution of v–r angles, the angle between the separation vector (r) and the relative velocity vector (v) of a wide binary (Hwang et al. 2022). This paper is structured as follows. Section 2 explains the sample selection. Section 3 presents the main results, showing that wide twin binaries are highly eccentric. We discuss the results and conclude in Section 4.

2. Sample Selection

The high-precision astrometry from Gaia (Gaia Collaboration et al. 2016) has enabled large-scale wide binary searches (Oh et al. 2017; El-Badry & Rix 2018; Hartman & Lépine 2020; Tian et al. 2020; Hwang et al. 2021). In this work, we use the ~1 million wide binaries within 1 kpc (El-Badry et al. 2021) selected from Gaia early Data Release 3 (eDR3; Gaia Collaboration et al. 2021). To avoid contamination, we require the chance-alignment probability to be <0.1 (El-Badry et al. 2021).

We use the v–r angle method to infer the eccentricity distribution of wide binaries (Tokovinin 1998, 2020; Tokovinin & Kiyawa 2016; Hwang et al. 2022). Qualitatively, the v–r angle distribution of randomly oriented circular binaries peaks at 90°, and the peak moves toward 0° and 180° for more-eccentric orbits (e.g., Figure 3 in Hwang et al. 2022). Quantitatively, Hwang et al. (2022) developed a Bayesian framework to derive the posterior of the underlying eccentricity distribution given a set of observed v–r angles, i.e., p(α|γ), where {α} are the free parameters of the eccentricity distribution and {γ} is a set of v–r angles. We refer the reader to Hwang et al. (2022) for the detail of the Bayesian framework.

The observed v–r angles of Gaia wide binaries are computed from the angle between the projected v and projected r vectors, where r is the vector connecting two member stars’ sky coordinates and v is the vector of two stars’ proper motion differences. We require that all wide binaries in the sample have angular separations >1″5 to avoid Gaia’s systematics on v–r angles in pairs below 1″25 (Hwang et al. 2022). To reliably measure v–r angles, we further limit the sample to have parallaxes >5 mas (i.e., distances <200 pc) and proper motion differences that are 3σ from being zero. With Gaia’s proper motion precision of ~0.1 mas yr^{-1}, simulations in Hwang et al. (2022) show that these selection criteria can recover 89.7% of 1000 au wide binaries’ proper motion differences at >3σ at distances of 200 pc, assuming that they are equal-solar-mass binaries with the so-called thermal eccentricity distribution (f(ε)dε = 2εde). All v–r angle measurements and related quantities used in this work are publicly available from Hwang et al. (2022).

With these selection criteria, the classification based on the absolute G-band magnitudes and BP–RP colors (binary_type in El-Badry et al. 2021) shows that 88% of the wide binaries with separations of 3000–10,000 au (hence angular separations >15°) are double main-sequence (MS) binaries, 10% are white dwarf (WD)–MS, and the rest are double-WD wide binaries. In Gaia eDR3, G-band photometry has an angular resolution of ~0.7″ (Fabricius et al. 2021). However, because BP and RP photometry does not have deblending treatment, BP and RP are not reliable for pairs <2″. For this reason, we do not use BP–RP colors to differentiate MS binaries from WDs in this work, but we expect the sample to be dominated (>90%) by MS–MS wide binaries.

Following El-Badry et al. (2019), we select wide twin binaries by ΔG < 0.25 mag, where ΔG is the difference in Gaia’s broadband photometry G of two component stars of a wide binary. For MS–MS binaries, ΔG < 0.25 mag corresponds to a mass-ratio selection of q > 0.95, with some slight dependence on the primary mass (El-Badry et al. 2019). Figure 1 shows the distributions of ΔG for different binary separations. Compared to binaries at >10,000 au, wide binaries ≤3000 au have an excess of twin binaries at ΔG < 0.25 mag. The median error of ΔG in our sample is 0.001 mag, much smaller than the width of the excess-twin component at ΔG ~ 0.25 mag.

Binaries selected by ΔG < 0.25 mag contain two components: one component is from the extension of the smooth, power-law-like mass-ratio distribution at q ≥ 0.5, and the other component is from the excess twins that only contribute to q ≤ q_{twin} ~ 0.95 (Moe & Di Stefano 2017; El-Badry et al. 2019). Here we use binaries at separations >10,000 au as the baseline where no significant excess twins are present (El-Badry et al. 2019) to quantify the fraction of excess twins at other separations. Specifically, binaries with ΔG < 0.25 mag constitute p_{ΔG<0.25} ≈ 7.70% ± 0.16% of all wide binaries at 400–1000 au, compared to p_{ΔG<0.25} ≥ 5.89% ± 0.36% at >10,000 au. Therefore, at ΔG < 0.25 mag and binary separations of 400–1000 au, the fraction of excess twins is
3. Wide Twin Binaries are Eccentric

Figure 2 shows the distribution of v–r angles for wide binaries with binary separations of 400–1000 au. Wide twin binaries (blue) are selected by ΔG < 0.25 mag, and wide nontwin binaries (orange) by ΔG > 0.25 mag. Figure 2 also shows that the simulated v–r angle distribution for circular binaries (solid black) with random orientation strongly peak at 90°, and the peaks move toward 0° and 180° for more-eccentric orbits (e.g., e = 0.9 for the dashed black line). The v–r angles of wide twin binaries are strongly enhanced at 0° and 180°, indicating the presence of highly eccentric binaries with e > 0.9. In contrast, wide nontwin binaries in this separation range have a flat v–r angle distribution, suggesting an underlying thermal eccentricity distribution (Hwang et al. 2022).

Using the Bayesian inference detailed in Hwang et al. (2022), we measure the eccentricity distributions of wide twin binaries as a function of projected binary separations (denoted by s). Specifically, we model the eccentricity distribution f(e) as a power law f(e) = (1 + ω)eα and obtain the best-fit α given the observed v–r angle distribution.

Figure 3 shows the best-fit power-law indices α for the eccentricity distributions of twin binaries (red) as a function of binary separations. For comparison, the black points and solid black line show the results from Hwang et al. (2022) for all wide binaries, which are dominated by nontwins; the red markers show α and separation bin sizes (horizontal) for the twin binaries. At 100–3000 au, twin binaries are significantly more eccentric (larger α) than other wide binaries at the same separations.

\[
E_{400-1000} = \frac{E_{3000-3000}}{E_{400}} = 23.5 \pm 5.1\%.
\]

Similarly, \[E_{400-1000} = (p_{400-1000} - p_{3000-3000})/p_{400} = 23.5 \pm 5.1\%.
\]

The v–r angle distributions of wide twin binaries (blue) are strongly enhanced at 0° and 180° compared to nontwins (orange), indicating the presence of highly eccentric twins with e > 0.9.
where $f_{\text{normal}}(e)$ and $f_{\text{ecc}}(e)$ are the eccentricity distributions for normal binaries and the excess eccentric binaries, respectively. At 400–1000 au, the nontwin ($\Delta G > 0.25$ mag) wide binaries have a flat $\nu$–$r$ angle distribution and its best-fit $\alpha$ is $1.05 \pm 0.05$, and therefore we adopt a thermal eccentricity distribution ($\alpha = 1$) for $f_{\text{normal}}(e) = 2e$ (Hwang et al. 2022). For excess eccentric binaries, we choose $f_{\text{ecc}}(e)$ as a top-hat function whose value is $1/(e_1 - e_0)$ between two free parameters $e_0$ and $e_1$, and zero elsewhere. With details shown in the Appendix, we use the affine-invariant Markov chain Monte Carlo (MCMC) ensemble sampler emcee (Foreman-Mackey et al. 2013) to constrain $F_{\text{ecc}}$, $e_0$, and $e_1$.

The best-fit parameters are $F_{\text{ecc}} = 0.189^{+0.042}_{-0.033}$, $e_0 = 0.948^{+0.021}_{-0.017}$, $e_1 = 0.992^{+0.004}_{-0.014}$. The best-fit values are the most probable values of the marginalized posterior distributions, and the uncertainties represent the highest posterior density interval that includes 68% of the area. Therefore, the observed $\nu$–$r$ angle distribution is best fit by $F_{\text{ecc}} = 18.9^{+3.2}_{-3.3}$% of highly eccentric ($e > e_0 = 0.948$) binaries among the twin binaries. The red dashed histogram in Figure 4 shows the simulated $\nu$–$r$ angle distribution of this model, well consistent with the observed distribution. The best fit of $f(e)$ (Equation (1)) in the right panel of Figure 4 illustrates the presence of highly eccentric twin binaries.

The median error of the $\nu$–$r$ angles for 400–1000 au twin binaries is $3.5^{\circ}$, meaning that the highest measurable eccentricity is $e = \cos(3.5^{\circ}) = 0.9983$ (Hwang et al. 2022). Therefore, our measured $e_1 = 0.992^{+0.004}_{-0.014}$ is approaching the precision limit. Despite the high eccentricities close to the hyperbolic regime ($e > 1$), the symmetric observed $\nu$–$r$ angle distribution in Figure 4 indicates that they are still on stable Keplerian orbits; otherwise, disrupting binaries on hyperbolic orbits would have $\nu$–$r$ angles enhanced at $0^{\circ}$ but not at $180^{\circ}$.

One natural explanation is that all excess twins identified from the mass-ratio distribution are highly eccentric. In this case, we would expect the twin excess fraction from the mass-ratio distribution to equal the fraction of the eccentric component, i.e., $E = F_{\text{ecc}}$. At separations 400–1000 au, the fraction of eccentric twins $F_{\text{ecc}} = 18.9^{+3.2}_{-3.3}$% is consistent with the excess-twin fraction at $\Delta G < 0.25$ mag measured from the $\Delta G$ (i.e., mass ratio) distribution, $E_{400-1000} = 23.5^{\pm} 5.1^{\%}$ (Section 2). However, with a similar analysis applying to twin binaries at 1000–3000 au, the fraction of eccentric twins is $F_{\text{ecc},1000-3000} = 21.6^{\pm} 3.9^{\%}$, which is much higher than $E_{1000-3000} = 4.0^{\%} \pm 4.8^{\%}$. Therefore, the connection between the excess in the mass-ratio distribution ($E$) and the excess in the eccentricity distribution ($F_{\text{ecc}}$) remains not fully established, and future work is needed to investigate if $F_{\text{ecc}}$ follows the same primary mass dependence as $E$ (El-Badry et al. 2019).

Figure 5 shows the eccentricity distribution power-law indices $\alpha$ versus $\Delta G$. For all separation bins between 100 and 3000 au, $\alpha$ strongly increases at $\Delta G < 0.25$ mag, the criterion used to select twin binaries. The marginal increase in $\alpha$ at $\Delta G = 0.25$–0.5 for binaries at 400–1000 au may hint that this bin still has some contribution from the eccentric twin binaries. At $\Delta G > 0.5$ mag, $\alpha$ becomes flat for all separation bins. Therefore, the high-eccentricity population is specifically for twin binaries ($\Delta G < 0.25$ mag), and the eccentricity

![Figure 4](image1.png) **Figure 4.** Left: the $\nu$–$r$ angle distributions for wide binaries at 400–1000 au (blue) and for simulated models (black and red). The best-fit power-law model of $\alpha = 2.14$ (dotted black) describes well the overall trend of twin binaries (solid blue) but with some noticeable differences. The dashed red line corresponds to 81.1% of normal wide binaries and 18.9% of $e = 0.948$–0.992 binaries, which agrees with the observation better than the power-law model. Right: the modeled eccentricity distribution (the dashed red line in the left panel) for twin binaries at separations 400–1000 au. The black shaded region shows the 20th–80th percentiles of the model.

![Figure 5](image2.png) **Figure 5.** The power-law indices $\alpha$ of eccentricity distributions ($f(e) \propto e^\alpha$) as a function of $\Delta G$. Only $\Delta G < 0.25$ mag has a significant increase in $\alpha$, suggesting that the high eccentricity is specifically associated with the twin excess, instead of a general trend with mass ratios.
distribution does not strongly depend on mass ratios anymore at \( \Delta G > 0.5 \text{ mag} \) \( (q \lesssim 0.9) \).

### 4. Conclusions and Discussion of Formation Channels

Wide twin binaries are a mysterious population that has near equal-mass ratios \((q > 0.95)\), common among close binaries, but has large binary separations of \(~\sim 10^4\) au. In this letter, using the \( v-r \) angle method to infer the eccentricity distribution (Hwang et al. 2022), we show that these wide twin binaries are highly eccentric (Figures 2, 3). Our result suggests that \( 18.9^{+2.1}_{-1.9}\% \) of wide twin binaries (selected by \( \Delta G < 0.25 \) mag) at \(~\sim 10^4\) au have eccentricities between \( e_0 = 0.948^{+0.021}_{-0.017} \) and \( e_1 = 0.992^{+0.004}_{-0.004} \) (Figure 4). Despite the high eccentricities, their symmetric \( v-r \) angle distribution with respect to 90° suggests that they are on stable Keplerian orbits, instead of being dissolving binaries. This high eccentricity is specific to excess twins, as opposed to being a smooth function of the mass ratio (Figure 5).

Binaries on eccentric orbits will most likely be observed near their apocenters where they spend most of their time due to the lower orbital velocities. For apocenters \( r_{apo} = 1000 \) au, the inferred eccentricities of \( e = 0.95 \) and \( 0.99 \) correspond to pericenters of \( r_{peri} = r_{apo}(1 - e)/(1 + e) = 26 \) au and 5 au, respectively. The high eccentricities of \(~\sim 10^4\) au wide twins must originate from their formation because interactions with passing stars and secular torquing by the Galactic tide mainly affect wide binaries at \(~\sim 10^5\) au, and the latter has been shown only to make the initial eccentricity distribution closer to thermal (Hamilton 2022). Pericenters smaller than the typical \(~\sim 100\) au sizes of circumbinary disks are consistent with the scenario in which twins are born with initial separations smaller than the size of the circumbinary disk, and they subsequently widen through dynamical interactions in the birth environments.

The nature of the dynamical interactions causing the wide and eccentric orbits remains uncertain. One approach to excite high eccentricities is an instantaneous velocity kick. To change a circular orbit with an orbital velocity \( v_{circ} \) to an eccentric orbit with \( e > 0.9 \), the required velocity kick \( v_{kick} \) is comparable with the original circular velocity \( (v_{kick} = v_{circ}(1 - \sqrt{1 - e}) \) ), where \( v_{circ} = 19 \text{ km s}^{-1} \) at 5 au. Therefore, an instantaneous kick with \( v_{kick} \sim 10 \text{ km s}^{-1} \) taking place in close binaries can produce eccentric \((e > 0.9)\) wide binaries. However, the source of such strong velocity kicks is currently not known in star formation processes. Protostellar outflows and jets can reach velocities of several 100 km s\(^{-1}\), but they are launched from the disk at the stage when the disk mass is only \(~\sim 10\%) of the central star (Bally 2016), and thus are unlikely to impose a strong kick on the star.

Chaotic three-body interactions can lead to the formation of close binaries with highly eccentric tertiary companions (Reipurth & Mikkola 2012). If the close binary was unresolved, the resulting triple system would look like a wide binary. However, radial velocity variations among wide twin binaries as well as the flux excess due to the unresolved companions suggest that unresolved companions are not more common in wide twins than in wide nontwins (El-Badry et al. 2019). Therefore, wide twin binaries are unlikely to form from chaotic three-body interaction.

For hierarchical triples that are not formed from chaotic three-body interaction, the resolved outermost companions would have less-eccentric orbits required by dynamical stability (Shatsky 2001; Tokovinin & Kiyava 2016; Hwang et al. 2022). Because the presence of unresolved companions can cause a nonzero \( \Delta G \), the equal-mass selection by \( \Delta G < 0.25 \) mag preferentially excludes systems with unresolved companions, thus allowing more-eccentric outer companions. In other words, we are investigating the possibility that wide twins are more eccentric than wide nontwins because unresolved companions are more common in wide nontwins. This scenario is possible because it is not uncommon to have unresolved companions in (predominantly nontwin) wide pairs (El-Badry et al. 2018; Hwang et al. 2020; Fezenko et al. 2022). To test this effect, we simulate the photometry of wide binaries using MIST (Choi et al. 2016; Dotter 2016) and brutus\(^7\) (J. S. Speagle et al. 2022, in preparation), where 50% of them are assumed to have unresolved companions and all component stars’ masses are drawn from the Kroupa initial mass function (Kroupa 2001). We find that \( \Delta G > 0.25 \) mag is only \(~\sim 5\%) more likely to have unresolved companions than \( \Delta G < 0.25 \) mag (for reference, \( \Delta G > 0.25 \) mag corresponds to a 1 \( M_\odot \) primary with an \( >0.79 \) \( M_\odot \) unresolved secondary. Note that the effect on \( \Delta G \) from an unresolved companion is different from the previous case of resolved binaries). Therefore, this potential effect from the lack of unresolved companions in wide twins is not able to explain \( F_{circ} = 18.9^{+2.1}_{-1.9}\% \) of high-eccentricity binaries at \( \Delta G < 0.25 \) mag.

Twin binaries may form through the enhanced accretion and interaction with circumbinary disks (Tokovinin & Moe 2020). Then, the strong interaction between binaries and the circumbinary disk may increase the binary’s eccentricity, even though the observed \( e > 0.95 \) is unusually high for typical disk–binary interaction in simulations (Artymowicz et al. 1991; Cuadra et al. 2009; Roedig et al. 2011). Alternatively, the process that widens binary orbits and causes high eccentricities may not be specific to twins. It is possible that such a process takes place among all close binaries, producing both eccentric wide twins and nontwins out to \(~\sim 10^4\) au. Then, because twins are more common in close binaries, the high-eccentricity component is more apparent in wide twins than wide nontwins. Future investigations are needed to establish the connection between close binaries, wide binaries, and their mass ratios and eccentricities.

Our results suggest that wide twin binaries have eccentricities approaching unity. Therefore, the process making these twin binaries wide and eccentric should also disrupt some of the binaries during the star formation. These disrupted binaries may contribute to the low-mass runaway or walkaway stars in star-forming regions (e.g., Schoettler et al. 2020), predicting a population of equal-mass runaway or walkaway pairs with opposite directions. Furthermore, some of these wide twin binaries may have pericenters comparable to or smaller than the radii of giant stars, which may lead to collision at later stellar evolution and the formation of blue stragglers (Kaib & Raymond 2014), although the twin fraction is lower in more massive stars where they can evolve to giants within the Hubble time (Moe & Di Stefano 2017; El-Badry et al. 2019).

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\(^7\) https://github.com/joshspeagle/brutus
and the dashed lines are the highest posterior density interval that includes 64% of the area.

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Appendix

Markov Chain Monte Carlo results

Our eccentricity model has three free parameters: $F_{\text{ecc}}$, $e_0$, and $e_1$ in Equation (1). According to Bayes’ theorem, their posterior distributions are

\[
p(e_0, e_1 | \{\gamma_{\text{obs,i}}\}) \propto p(F_{\text{ecc}}) p(e_0)p(e_1) \Pi_i \times \int p(\gamma_{\text{obs,i}} | \gamma_{\text{true},i}) p(\gamma_{\text{true},i}|e_1) p(e_1) \text{d} \gamma_{\text{true},i} \text{d} e_1,
\]

where $i$ is the index of individual binaries, $\gamma_{\text{obs,i}}$ is the observed $v-r$ angle for binary $i$, and $p(\gamma_{\text{obs,i}} | \gamma_{\text{true},i})$ is the error distribution for $v-r$ angles. To probe the high eccentricity model close to 1, we use binary simulations to compute the $p(\gamma_{\text{true},i}|e_1)$ for eccentricities from 0 to 1 with a step of 0.001 and $\gamma_{\text{true},i}$ with a step of 0.5. The details of these terms can be found in Hwang et al. (2022).

We then use emcee to derive the posterior distributions. In the MCMC run, we numerically compute the two-dimensional integral in Equation (A1) with equal spacings of $\Delta \varepsilon = 0.001$ and $\Delta \gamma = 0^\circ.5$. Uninformative flat priors are adopted for $p(e_0)$, $p(e_1)$, and $p(F_{\text{ecc}})$, and we further require that $e_1 > e_0$. We use the Gaussian move as the proposal function in the MCMC to mitigate the effect of finite $\Delta \varepsilon$ in the integral calculation. The resulting posterior distributions for 400–1000 au wide twin binaries are shown in Figure A1 (Foreman-Mackey 2016).

References

Andrews, S. M., Huang, J., Pérez, L. M., et al. 2018, ApJL, 869, L41
Ansdel, M., Williams, J. P., Trappman, L., et al. 2018, ApJ, 859, 21
Artymowicz, P., Clarke, C. J., Lubow, S. H., & Pringle, J. E. 1991, ApJL, 370, L35
Artymowicz, P., & Lubow, S. H. 1994, ApJ, 421, 651
Bally, J. 2016, ARA&A, 54, 491
Bate, M. R., & Bonnell, I. A. 1997, MNRAS, 285, 33
Choi, J., Dotter, A., Conroy, C., et al. 2016, ApJ, 823, 102
Cuahua, J., Armitage, P. J., Alexander, R. D., & Begelman, M. C. 2009, MNRAS, 393, 1423
Dittmann, A. J., & Ryan, G. 2022, MNRAS, 513, 6158
Dotter, A. 2016, ApJS, 222, 8
Duffell, P. C., D’Orazio, D., Derdzinski, A., et al. 2020, ApJ, 901, 25
El-Badry, K., & Rix, H.-W. 2018, MNRAS, 480, 4884
El-Badry, K., Rix, H.-W., & Heintz, T. M. 2021, MNRAS, 506, 2269
El-Badry, K., Rix, H.-W., Tian, H., Duchêne, G., & Moe, M. 2019, MNRAS, 489, 5822
El-Badry, K., Ting, Y.-S., Rix, H.-W., et al. 2018, MNRAS, 476, 528
Fabricius, C., Luri, X., Arenou, F., et al. 2021, A&A, 649, A5
Farris, B. D., Duffell, P., Macfadyen, A. I., & Haiman, Z. 2014, ApJ, 783, 134
Fezenko, G. B., Hwang, H.-C., & Zakamska, N. L. 2022, MNRAS, 511, 3881
Foreman-Mackey, D. 2016, IOPSS, 1, 24
Foreman-Mackey, D., Hogg, D. W., Lang, D., & Goodman, J. 2013, PASP, 125, 306
Gaia Collaboration, Brown, A. G. A., Vallenari, A., et al. 2021, A&A, 649, A1
Gaia Collaboration, Prusti, T., de Bruijne, J. H. J., et al. 2016, A&A, 595, A1
Hamilton, C. 2022, ApJL, 929, L29
Hartman, Z. D., & Lépine, S. 2020, ApJ, 827, 66
Heath, R., & Nixon, C. 2020, A&A, 641, A64
Hwang, H.-C., Hamer, J. H., Zakamska, N. L., & Schlaufman, K. C. 2020, MNRAS, 497, 2250
Hwang, H.-C., Ting, Y.-S., & Schlaufman, K. C., Zakamska, N. L., & Wyse, R. F. 2021, MNRAS, 501, 4329
Huang, H.-C., Ting, Y.-S., & Zakamska, N. L. 2022, MNRAS, 512, 3383
Kaib, N. A., & Raymond, S. N. 2014, ApJ, 783, 102
Kroupa, P. 2001, MNRAS, 322, 231
Lucy, L. B., & Ricco, E. 1979, AJ, 84, 401
Manara, C. F., Tazzari, M., Long, F., et al. 2019, A&A, 628, A95
Miranda, R., Muñoz, D. J., & Lai, D. 2019, ApJ, 871, 84
Moe, M., & Di Stefano, R. 2017, ApJS, 230, 15
Moody, M. S. L., Shi, J.-M., & Stone, J. M. 2019, ApJ, 875, 66
Muñoz, D. J., Miranda, R., & Lai, D. 2019, ApJ, 871, 84
Ochi, Y., Sugimoto, K., & Hanawa, T. 2005, ApJ, 623, 922
Oh, S., Price-Whelan, A. M., Hogg, D. W., Morton, T. D., & Spelberg, D. N. 2017, AJ, 153, 257
Pichardo, B., Sparke, L. S., & Aguilar, L. A. 2005, MNRAS, 359, 521
Ragusa, E., Alexander, R., Calcino, J., et al. 2020, MNRAS, 499, 3362
Reipurth, B., & Tokovinin, A. 2016, MNRAS, 456, 2070
Schoettler, C., De Bruijne, J., Vaahes, E., & Parker, R. J. 2020, MNRAS, 495, 3104
Shatsky, N. 2001, A&A, 380, 238
Shi, J.-M., Krolik, J. H., Lubow, S. H., & Hawley, J. F. 2012, ApJ, 749, 118
Soderhjelm, S. 2007, A&A, 463, 683
Tian, H.-J., El-Badry, K., Rix, H.-W., & Gould, A. 2020, ApJS, 246, 4
Tiede, C., Zrake, J., MacFadyen, A., & Haiman, Z. 2020, ApJ, 900, 43
Tokovinin, A. 2020, MNRAS, 496, 993
Tokovinin, A., & Kiyavichas, O. 2016, MNRAS, 456, 2070

The Astrophysical Journal Letters, 933:L32 (7pp), 2022 July 10
Hwang et al.
Tokovinin, A., & Moe, M. 2020, MNRAS, 491, 5158
Tokovinin, A. A. 1998, AstL, 24, 178
Tokovinin, A. A. 2000, A&A, 360, 997

Young, M. D., Baird, J. T., & Clarke, C. J. 2015, MNRAS, 447, 2907
Young, M. D., & Clarke, C. J. 2015, MNRAS, 452, 3085