Based on Fluent Numerical Calculation of Refractive Index on Rocket Engine Nozzle Plume

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ABSTRACT
Numerical 2D simulation and research on internal flow field and external flow field of rocket motor nozzle using FLUENT software. Analyze the flow condition of internal flow field and external flow field, and according to add in the amount of the different gas components, obtain the clear distribution of contour of density flow field, pressure flow field and various material components and so on. Simulation results agree with the results observed from the test on the ground, and provide reference for solid rocket motor development.

Keywords: Rocket Engine Nozzle; Nozzle Plume; Fluent; Numerical Simulation

1. Introduction
The plume of the rocker motor is composed by the high temperature, high-pressure, high-flow combustion products of propellant, which go though Laval-nozzle flow by static state and form a supersonic gas flow on the cross section of a nozzle. The exhaust plume of rocket motor nozzle is composed by H₂O, CO₂, CO, H₂ and N₂ and so on. According to design conditions of the difference, they will make larger difference among flow field calculation, so in order to obtain the best density field contours, here we chose the parameters of 7500 N thrust for numerical calculation. In this paper, some propellant was thermodynamically calculated, and the total temperature and the total pressure of the gas and the mass fraction of the ingredients of combustion resultants were obtained. Meanwhile, the finite-rate chemical reaction model of flow field of exhaust plume was built. Using fluent calculation software solve the NS equation and the component transport equation, so temperature field and density field and ingredient distribution curves of the exhaust plume were calculated, then the relationship of making use of density field and several ingredient contents solve the distribution of refractive index field which compare with the experimental results again, it is available to verify the calculation method.

2. Calculation Conditions and Boundary Condition
In order to numerical calculation which is convenient, some rocket motor model is predigested processing. Selecting the combustor end which is the nozzle inlet is also the gas inlet. In order to obtain higher calculation accuracy, the compressible, Reynolds-averaged difference N-S equation and second order upwind are adopted to solve the model when calculating internal flow field and nozzle plume area. The turbulence model will adopt RNG k-ε equation [1] turbulence model, and using non-equilibrium wall function [2] near the wall is processing. The calculation method will adopt PISO algorithm which must solve the pressure correction equation twice. So it needs additional storage space to calculate the source term in the secondary pressure correction equation. Although this method involves more calculations, compared to other algorithms, its speed fast, iteration converges faster, and efficiency is very high.

2.1. Computational Domain and Boundary Conditions
Computational domain of nozzle and flow field of plume is shown in Figure 1. Effective length of the plume domain is about 10 m × 3 m. The ABHI area is the terminal area of combustion chamber which is also nozzle area, the EFGH area and the CDEHB area are plume...
ones. The boundaries of the computational domain are divided as following: AI area is boundary condition of the entrance of engine nozzle; AC area is symmetrical axis of the computational domain; CD, DEF and FG area are boundary conditions of the exit of engine nozzle; GH and HI area are wall conditions. The boundary condition of the entrance of engine nozzle can be obtained with the thermodynamic calculation under the working condition of 7500 N thrust, which includes the total pressure 0.8 MPa, the total temperature 3040K, and the mass fraction of the ingredient of combustion resultant as shown in Table 1; the total pressure $1.01325 \times 10^5$ Pa and the total temperature 300 K as the boundary condition of the exit of engine nozzle; Viscous no-slip boundary was chosen as the boundary condition of the inner wall surface of engine nozzle.

### 2.2. Mesh Dividing of the Computational Domain

According to the status of the gas flowing within the nozzle, closing to the wall within the nozzle and symmetrical axis in plume domain are taken to mesh refinement, the computational mesh needs to adopt the division of structured mesh. The setup of computational region and the division of computational meshes are shown in Figure 2.

### 3. Numerical Computation Approach

Under normal circumstances, the relationship between the density of plumes ($\rho$) and the refractive index of plumes ($n$) can make use of the Gladstone-Dale [6] formula which can be expressed as

$$ n = 1 + \sum_i K_i \alpha_i \rho $$

where $K_i$ are a property of the gases and are also the Gladstone-Dale constants, called as refractivity. By looking up table we obtain $K_i$ of the five main components of plumes which are given in Table 2; $\alpha_i$ are the mass fractions of the individual components; $\rho$ is the density of plumes.

### 4. Computation Results and Analysis

In the paper, the nozzle inflow medium can be considered as the gas of ambient temperature which is treated as idea status. Viscosity coefficient using the three-coefficient Sutherland method is calculated [3]. The flow model is numerical calculated by using FLUENT software. Through simulated calculation solve the differential N-S equation [4], the internal field and external field of engine motor nozzle are obtained. The distribution of the contour of the density is shown in Figure 3; the distribution of the contour of the total pressure is shown in Figure 4; the distribution of the contour of the temperature is shown in Figure 5; and the distribution of the contour of axial velocity and radial velocity are shown in Figures 6(a) and (b) respectively; the distribution of the contour of mass fractions of five main components computed are shown in Figures 7(a), (b), (c), (d) and (e) respectively.

We can see from Figure 3 to Figure 6 that the density and the pressure of the external field of motor plume are higher in place of the entrance cross section of particles,

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**Table 1.** Mass fraction of the ingredients of combustion resultant in the entrance of the nozzle.

| Sequence | Ingredient | Mass fraction |
|----------|------------|---------------|
| 1        | H$_2$      | 0.0144        |
| 2        | CO$_2$     | 0.0832        |
| 3        | CO         | 0.1746        |
| 4        | H$_2$O     | 0.2866        |
| 5        | N$_2$      | 0.4160        |

**Table 2.** Gladstone-Dale constants of the five main components of plumes.

| Sequence | Ingredient | $K_i$  |
|----------|------------|--------|
| 1        | H$_2$      | 1.538  |
| 2        | CO$_2$     | 0.229  |
| 3        | CO         | 0.267  |
| 4        | H$_2$O     | 0.312  |
| 5        | N$_2$      | 0.238  |
Figure 3. The distribution of the contour of the density.

Figure 4. The distribution of the contour of the total pressure.

Figure 5. The distribution of the contour of the temperature.

Figure 6. (a) The distribution of the contour of axial velocity; (b) The distribution of the contour of radial velocity.

Figure 7. (a) The distribution of the contour of mass fractions of H\textsubscript{2}; (b) The distribution of the contour of mass fractions of CO\textsubscript{2}; (c) The distribution of the contour of mass fractions of CO; (d) The distribution of the contour of mass fractions of H\textsubscript{2}O; (e) The distribution of the contour of mass fractions of N\textsubscript{2}.
but reduced with air stream flowing to the vacuum; the higher the temperature, the faster the particle’s velocity, and with the expansion of jet flow and continue to rise, temperature does not rise after gas flow diffuse into the plume field; the axial velocity is the smallest one through the exit cross section of motor, but radial velocity is the biggest one, basically the distribution of velocity along radial direction and increase constantly, and show a diffusing accelerated process.

We can see from Figure 7 that the mass fractions of the five individual components are changed constantly with gases flowing into motor plume.

The above analysis shows that the main impact in the motor plume flow field is that come from the diffusion of boundary layer in the exit wall boundary of motor; plume in vacuum diffuses very fast, and the ability of doing work decrease greatly; the refractive index field will have an influence with gas flow diffusion.

5. Conclusions

This paper mainly calculated the refractive index field of rocket motor nozzle plume, and two-dimensional axisymmetric Reynolds averaged NS equation was chosen to solve; this paper that using FLUENT software carried out numerical simulation which analyzed detailed conditions and distribution characteristics of internal field and external field of nozzle. At the same time, related fluid flow theory was verified. This simulation provided the data base in aspects of the design of rocket motor and carrying out other researches for plume flow field. Other parts need to be further study.

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