DETERMINATION OF PULSATION FACTORS OF THE SYSTEM OF SUPPRESSION OF INTERFERING HARMONICS OF A SEMICONDUCTOR CONVERTER

Purpose. The purpose of the paper is to define the pulsation factors of a closed-loop automatic control system (ACS) of interfering harmonics containing a semiconductor converter with double-sided pulse-width modulation (PWM), as well as confirmation of theoretical assumptions about possibilities of self-compensation of pulsation factors’ influence in the system with double-sided PWM. Methodology. The research was conducted with the usage of classic electric circuit theory, frequency analysis methods, generalized function theory. Results. The obtained expressions mathematically relate pulsation factors, value of the damping coefficient and manipulative variable for different frequencies of interfering harmonics in the system with double-sided PWM. The research concerned harmonics with frequencies 100, 300, 600, 900 and 1200 Hz as the most significant constituents of the output voltage of a 12-pulse semiconductor converter. The obtained expressions allow taking into account settings of the selective link and its approximation on the level of supreme frequencies with aperiodic link. Originality. The research has experimentally proved theoretical assumptions about self-compensation of pulsation factors in the system with double-sided PWM. It has been shown that the damping coefficient has a lowimpact influence on the values of pulsation factors. It is caused by the pass band of the selective link, which is included in the closed-loop control system of harmonics regulation. Practical value. Application of the research results can contribute to the development of the closed-loop control system for effective attenuation of interfering harmonics in direct current contact wire without interfering in the power part of the semiconductor converter. Besides the possibility to regulate output voltage, it will also help to solve the problem of electromagnetic compatibility of a traction substation semiconductor converter with contact wire. The application of the developed closed-loop control system will as well provide for decreasing the size of the filter in the direct current traction substation unit. References 9, figures 5.

Key words: pulsation factor, interfering harmonic, automatic control system, double-sided pulse-width modulation, semiconductor converter.

Цель. Целью статьи является определение факторов пульсаций замкнутой системы автоматического регулирования (САР) мешающих гармоник, содержащей полупроводниковый преобразователь с двухсторонней широтно-импульсной модуляцией (ШИМ), а также подтверждение теоретических предпосылок о возможности самокомпенсации действия факторов пульсаций в системе с двухсторонней ШИМ. Методика. Для проведения работы использовались: классическая теория электрических цепей, методы гармонического анализа и теория обобщенных функций. Результаты. Получены выражения, математически связывающие факторы пульсаций, значения коэффициентов демпфирования и регулируемого параметра для разных частот мешающих гармоник в системе с двухсторонней ШИМ. Научная новизна. Экспериментально подтверждены теоретические предпосылки о самокомпенсации действия факторов пульсаций в системе с двухсторонней ШИМ; Практическое значение. Использование результатов работы позволит создать замкнутую САР для эффективного подавления мешающих гармоник в контактной сети постоянного тока. Библа. 9, рис. 5.

Ключевые слова: фактор пульсаций, мешающая гармоника, система автоматического регулирования, двухсторонняя широтно-импульсная модуляция, полупроводниковый преобразователь.

Problem definition. The main disadvantages of semiconductor converters with increased pulsation are:

- impossibility to create a converter with absolutely symmetrical shoulders, which leads to generation of harmonics, reduction of the quality of electric energy at the output of the traction substation and deterioration of the electromagnetic compatibility of the rectifier with the traction network. The problems of symmetrization of semiconductor converters remain unsolved in [1, 2];

- constant presence of non-canonical harmonics in output voltage, to which signaling, centralization and blocking (SCB) devices are critical and which do not depend on rectifier pulsation, due to the practical impossibility of creating an integer ratio of turns of high power transformer windings supplying rectifier bridges. At the same time, in [3, 4], the possibility of applying active filtering of harmonics of the output voltage of a semiconductor converter is not considered.

In addition, the cause of the disturbing harmonics is the discrete nature of the rectification conversion of the electric energy of the alternating current and the effect of the inherent asymmetry of the rectifier and the asymmetry of the supply network. These reasons cause the generation into the contact network of canonical and non-canonical harmonics. A large contribution to the formation of an interfering voltage is made by harmonics whose frequencies lie in the range $f_m = 100...1200$ Hz. The use to reduce the amount of interfering harmonics in the specified range in the composition of the smoothing filter of rejection $LC$ circuits is not effective enough [5, 6]. This is explained by the difficulty of obtaining precise tuning of the rejection circuits at the frequencies of the interfering harmonics and changing the resonant frequencies caused by the temperature and time effects.

That is, it is actual to search for alternative technical solutions for combating the interfering harmonics of a semiconductor converter.

In [7] the questions of application of special closed structures for regulating the harmonics of the output voltage of the controlled converter were considered. However, the proposed systems with single-sided PWM
The use of a two-sided PWM instead of a one-sided PWM is due to the possibility of extending the converter bandwidth, which will suppress the harmonics of the output voltage of a DC traction substation over a wide frequency range, and therefore reduce the volume of the PF.

In the booster converter, the formation of a pulse-width modulated pulse train is performed by a control system, the functional circuit of which is shown in Fig. 2. Functionally, the control system consists of a reference voltage generator RVG and a comparator K.

![Fig. 2. Functional circuit of the control system](image)

In [8] generalized expressions for the pulsation factors were obtained in the representation of the transfer function of the reduced continuous part as a sum of aperiodic links. For the system for suppressing the interfering harmonic, the expressions for the pulsation factors have the form

\[
F_1^{-1} = 1 - \sum_{i=1}^{n} K_p T_i \frac{(1 - e^{-T_i})}{T_i} , \quad (1)
\]

\[
F_2^{-1} = 1 + \sum_{i=1}^{n} K_p T_i \frac{(1 - e^{-T_i})}{T_i} . \quad (2)
\]

To apply formulas (1), (2), we represent the transfer function of the selective link \( G(p) \) as a sum of aperiodic links

\[
G(p) = \frac{p}{T_0} \left( \frac{K_1}{p-p_1} + \frac{K_2}{p-p_2} \right) , \quad (3)
\]

where \( p_1 = (-\xi + ja)/T_0, \ p_2 = (-\xi - ja)/T_0 \) are the poles of the transfer function \( G(p) \).

The coefficients \( K_1 \) and \( K_2 \) are defined as the residues of the transfer function \( G(p) \) in the corresponding poles

\[
K_1 = \left| \frac{p}{p-p_2} \right|_{p=p_1} = \frac{a+j\xi}{2a} , \quad (4)
\]

\[
K_2 = \left| \frac{p}{p-p_2} \right|_{p=p_2} = \frac{a-j\xi}{2a} . \quad (5)
\]

Substituting (4) and (5) into (3) and transforming, we obtain

\[
G(p) = \frac{j}{2a} \left[ \frac{1}{T_0(\xi + ja)+1} - \frac{1}{T_0(\xi - ja)+1} \right] . \quad (6)
\]

Taking into account (6), the expressions for the pulsation factors take the form
Performing simple but rather cumbersome transformations in (7) and (8), we obtain expressions for the pulsation factors of the closed system for suppressing the interfering harmonics

\[ F_1^{-1} = 1 - j \frac{K_p T_1}{4aT_0} \begin{pmatrix} (\xi - ja) \frac{T_1}{T_0} - (\xi - ja) \frac{T_1}{T_0} \\ (\xi + ja) \frac{T_1}{T_0} - (\xi + ja) \frac{T_1}{T_0} \end{pmatrix}, \quad (7) \]

\[ F_2^{-1} = 1 + j \frac{K_p T_1}{4aT_0} \begin{pmatrix} (\xi - ja) \frac{T_1}{T_0} - (\xi - ja) \frac{T_1}{T_0} \\ (\xi + ja) \frac{T_1}{T_0} - (\xi + ja) \frac{T_1}{T_0} \end{pmatrix}, \quad (8) \]

Performing simple but rather cumbersome transformations in (7) and (8), we obtain expressions for the pulsation factors of the closed system for suppressing the interfering harmonics

\[ F_1^{-1} = 1 + j \frac{K_p T_1}{2aT_0} \begin{pmatrix} \frac{T_1}{T_0} - C_{1,1} e^{-\xi(1-\gamma) \frac{T_1}{T_0}} \\ 1 - 2e^{-\frac{T_1}{T_0} \cos \alpha} \frac{T_1}{T_0} + e^{-2\xi \frac{T_1}{T_0}} - C_{1,2} e^{\xi(2-\gamma) \frac{T_1}{T_0} + a \cdot e} \end{pmatrix}, \quad (9) \]

where

\[ C_{1,1} = \xi \sin \alpha \frac{T_1}{T_0} - a \cos \alpha \frac{T_1}{T_0}; \]

\[ C_{1,2} = \xi \sin \alpha(1-\gamma) \frac{T_1}{T_0} - a \cos \alpha(1-\gamma) \frac{T_1}{T_0}; \]

\[ C_{1,3} = \xi \sin \alpha \gamma \frac{T_1}{T_0} - a \cos \alpha \gamma \frac{T_1}{T_0}; \]

\[ F_2^{-1} = 1 - \frac{K_p T_1}{2aT_0} \begin{pmatrix} \frac{T_1}{T_0} - C_{2,1} e^{-\xi \gamma \frac{T_1}{T_0}} \\ 1 - 2e^{-\frac{T_1}{T_0} \cos \alpha} \frac{T_1}{T_0} + e^{-2\xi \frac{T_1}{T_0}} - C_{2,2} e^{\xi(1-\gamma) \frac{T_1}{T_0} + a \cdot e} \end{pmatrix}, \quad (10) \]

where

\[ C_{2,1} = \xi \sin \alpha \gamma \frac{T_1}{T_0} - a \cos \alpha \gamma \frac{T_1}{T_0}; \]

\[ C_{2,2} = \xi \sin \alpha \gamma \frac{T_1}{T_0} - a \cos \alpha \frac{T_1}{T_0}; \]

\[ C_{2,3} = \xi \sin \alpha(1-\gamma) \frac{T_1}{T_0} + a \cos \alpha(1-\gamma) \frac{T_1}{T_0}. \]

Fig. 3, 4 show the results of calculating the pulsation factors for different values of the controlled parameter \( \gamma \), the damping coefficient \( \xi \), and the frequencies of the interfering harmonics.

From the obtained dependences it follows that in contrast to a system with one-sided pulse-width modulation in a system with two-way pulse-width modulation, the effect of self-compensation of the action of pulsation factors is observed. There is a weak dependence of the pulsation factors on the damping coefficient. This is explained by the fact that the frequencies influencing the values of the pulsation factors lie outside the pass band of the selective link.
The amplitude-frequency response of the selective link \( G(p) \) in the region of higher frequencies has a slope of -20 dB/dec. This gives a prerequisite for the approximation of the link \( G(p) \) by an aperiodic link

\[
H(p) = \frac{1}{T_c p + 1},
\]

having the same transmission factor as \( G(p) \) at the pulse-width modulation frequency.

The time constant of an aperiodic link is defined as

\[
T_c^2 = \frac{1 + \frac{f_{PWM}^2}{f_q^2} \left[ \frac{f_{PWM}^2}{f_q^2} \left(1 - 2\xi^2\right) - 2\xi^2\right] - 1}{4\pi^2 \frac{f_{PWM}^4}{f_q^4}},
\]

where \( f_{PWM} \) is the pulse-width modulation frequency; \( f_q \) is the frequency of the \( q \)-th interfering harmonic.

In this case, the expressions for the pulsation factors take the form [6]:

\[
F_1^{-1} = 1 - K_p T_1 \frac{(1 - e^{-\frac{T_1}{T_e}} e^{-\frac{T_2}{T_e}})}{1 - e^{-\frac{T_1}{T_e}}};
\]

\[
F_2^{-1} = 1 + K_p T_1 \frac{e^{-\frac{T_1}{T_e}} - e^{-\frac{T_2}{T_e}}}{1 - e^{-\frac{T_1}{T_e}}},
\]

Fig. 5 shows the graphical dependencies characterizing the changes in the pulsation factor in the function of the regulated parameter \( \gamma \), calculated from formulas (13) and (14).

**Conclusions.**

For the first time, expressions were obtained for determining the pulsation factors of the automatic control system of interfering harmonics of a semiconductor converter with a two-way PWM for different values of the damping coefficient and the controlled parameter.

It is established that in the considered automatic control system of a semiconductor converter with two-way PWM, self-compensation of the action of pulsation factors occurs.

As a result of the investigation of electromagnetic processes in the automatic control system of a semiconductor converter, the possibility of suppressing interfering harmonics without interference in its power part was revealed. This is especially important in the maintenance of the rectifying installation of the traction substation.

**REFERENCES**

1. Richter J., Doppelbauer M. Control and mitigation of current harmonics in inverter-fed permanent magnet synchronous machines with non-linear magnetics. IET Power
2. Ghanizadeh R., Ebadian M., Gharehpetian G.B. Non-linear load sharing and voltage harmonics compensation in islanded microgrids with converter interfaced units. *International Transactions on Electrical Energy Systems*, 2016, vol.27, no.1, p. e2237. doi: 10.1049/iet-pel.2015.0977.

3. Panchenko V.V. The harmonic composition of the output voltage of a rectifier unit with a PWM voltage booster converter. *Information and control systems at railway transport*, 2015, no.4, pp. 71-78. (Rus).

4. Kuznetsov B.I., Nikitina T.B., Tatarchenko M.O., Khomenko V.V. Multicriterion anisotropic regulators synthesis by multimass electromechanical systems. *Technical Electrodynamics*, 2014, no.4, pp. 105-107. (Rus).

5. Sozanski K. Three phase active power filter with selective harmonics elimination. *Archives of Electrical Engineering*, 2016, vol.65, no.1, pp. 33-44. doi: 10.1515/aeec-2016-0003.

6. Huang J., Shi H. Suppression of the Peak Harmonics from Loads by Using a Variable Capacitance Filter in Low-Voltage DC/DC Converters. *IEEE Transactions on Electromagnetic Compatibility*, 2016, vol.58, no.4, pp. 1217-1227. doi: 10.1109/temc.2016.2552230.

7. Coillot C., Nativel E., Zanca M., Goze-Bac C. The magnetic field homogeneity of coils by means of the space harmonics suppression of the current density distribution. *Journal of Sensors and Sensor Systems*, 2016, vol.5, no.2, pp. 401-408. doi: 10.5194/jsss-5-401-2016.

8. Scherbak Y.V., Ivakina K.Y., Panchenko V.V. Factor pulsations automatic regulation with two-way pulse width modulation. *Collected scientific works of Ukrainian State University of Railway Transport*, 2015, no.153, pp. 113-120. (Rus). doi: 10.18664/1994-7852.153.2015.0436.

9. Panchenko V.V. Dynamic properties of system «rectifier with buck converter – load». *East-European Journal of Enterprise Technologies*, 2013, vol.4, no.8(64), pp. 14-17. (Ukr).

Received 12.04.2018

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*How to cite this article:* Panchenko V.V., Maslii A.S., Pomazan D.P., Buriakovskyi S.G. Determination of pulsation factors of the system of suppression of interfering harmonics of a semiconductor converter. *Electrical engineering & electromechanics*, 2018, no.4, pp. 24-28. doi: 10.20998/2074-272X.2018.4.04.