Double X/Peanut Structures in Barred Galaxies – Insights from an $N$–body Simulation

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ABSTRACT

Boxy, peanut– or X–shaped “bulges” are observed in a large fraction of barred galaxies viewed in, or close to, edge-on projection, as well as in the Milky Way. They are the product of dynamical instabilities occurring in stellar bars, which cause the latter to buckle and thicken vertically. Recent studies have found nearby galaxies that harbour two such features arising at different radial scales, in a nested configuration. In this paper we explore the formation of such double peanuts, using a collisionless $N$–body simulation of a pure disc evolving in isolation within a live dark matter halo, which we analyse in a completely analogous way to observations of real galaxies. In the simulation we find a stable double configuration consisting of two X/peanut structures associated to the same galactic bar – rotating with the same pattern speed – but with different morphology, formation time, and evolution. The inner, conventional peanut-shaped structure forms early via the buckling of the bar, and experiences little evolution once it stabilises. This feature is consistent in terms of size, strength and morphology, with peanut structures observed in nearby galaxies. The outer structure, however, displays a strong X, or “bow-tie”, morphology. It forms just after the inner peanut, and gradually extends in time (within 1 to 1.5 Gyr) to almost the end of the bar, a radial scale where ansae occur. We conclude that, although both structures form, and are dynamically coupled to, the same bar, they are supported by inherently different mechanisms.

Key words:
galaxies: structure – galaxies: bulges – galaxies: evolution – galaxies: kinematics and dynamics

1 INTRODUCTION

Barred galaxies often display boxy, X– or peanut–shaped “bulges” when observed in an edge-on orientation of their stellar disc. Unlike conventional, axisymmetric galaxy bulges – either built secularly from the disc (typically oblate and rotating “pseudobulges”), or constituting the remnants of past mergers (spheroidal classical bulges) – X/peanut (X/P) structures are believed to be the vertically thickened and non-axisymmetric inner parts of bars. Early studies with $N$–body simulations have shown that peanuts arise naturally from bars as the latter experience vertical (i.e., perpendicular to the disc plane) resonances, particularly the vertical 2:1 inner Lindblad resonance (vILR) (Combes & Sanders 1981, Combes et al. 1990) or buckling instabilities (Raha et al. 1991, Merritt & Sellwood 1994, Martinez-Valpuesta, Knapen & Buta 2007), and can have a significant effect on their host galaxies (Fragkoudi et al. 2015, Fragkoudi, Athanassoula & Bosma 2016). In parallel, the (bar–peanut) connection has been extensively supported observationally (Shaw 1987, Dettmar & Barteldrees 1990, Kuijken & Merrifield 1995, Bureau & Freeman 1999, Bureau & Athanassoula 2005), with Erwin & Debattista (2016) recently showing observations of galaxy bars in the act of buckling to form...
peanut structures. The field has advanced sufficiently in recent times to perform systematic studies on the X/P host galaxy population. Erwin & Debattista (2017) have shown that the incidence of X/P structures in barred galaxies is a strong function of their host’s stellar mass and Hubble type (the fraction being higher in more massive, and earlier–type, disc galaxies), while more recently the frequency of occurrence of X/P structures has been probed as a function of redshift, from observations ranging from the local Universe out to \( z \approx 1 \) (Kruk et al. 2019), as well as in cosmological simulations (Fragkoudi et al. 2019). As a rather typical spiral barred galaxy, the Milky Way too displays a peanut–shaped “bulge” (Okuda et al. 1977, Dwek et al. 1995, Binney, Gerhard & Spergel 1997, Babusiaux & Gilmore 2005, López-Corredoira, Cabrera-Lavers & Gerhard 2005, Gerhard 2015, Gonzalez & Gadotti 2016, Ness & Lang 2016), and our privileged placement within its disk has allowed us to study its bulge in exquisite detail, in terms of its large-scale morphology in the near-infrared (Ciambur, Graham & Bland-Hawthorn 2017), or as inferred through tracers (McWilliam & Zoccali 2010, Ness et al. 2012, López-Corredoira, Cabrera-Lavers & Gerhard 2005, Wegg, Gerhard & Portail 2015). Stellar population studies have shown that the vast majority of stars in the Galactic bulge originate from the disc (Shen et al. 2010, Ness et al. 2013, Di Matteo et al. 2014, Di Matteo 2016, Fragkoudi et al. 2017c, Fragkoudi et al. 2018), further support for its formation through a secular channel.

X/P structures leave a measurable imprint in the light distribution of galaxies, specifically in the 6th order Fourier harmonic (the cosine term coefficient, \( B_6 \)) of the one-dimensional intensity distribution along an isophote. Exploiting this, Ciambur & Graham (2016), hereafter CG16, have introduced a framework to extract quantitative parameters of X/P structures, such as size and strength, directly from galaxy images. Applying this method on a sample of twelve nearby galaxies previously known in the literature to host peanut–shaped bulges, they showed that the X/P parameters are correlated and broadly define structural scaling relations. Interestingly, two galaxies in this sample, NGC 128 and NGC 2549, were found to host a double, nested peanut configuration, i.e., a small scale X/P bulge embedded within a larger one. While only recently simulations of barred galaxies are seen to develop double X–shaped features under certain circumstances (e.g., Debattista et al. 2017, Smirnov & Sotnikova 2018, Parul, Smirnov & Sotnikova 2020), the face–value interpretation of CG16 at the time was that each of the two co-existing X/P structures is associated with a distinct bar component, as double bar galaxies had been known for long to occur (Friedli et al. 1996, Erwin et al. 2001, Erwin 2011). Indeed, in a recent paper Méndez-Abreu et al. (2019) have detected a double peanut configuration in the face–on galaxy NGC 1291 (using the face–on signature of peanut galaxies, as introduced in Debattista et al. 2005), which indeed hosts a large–scale, and a second embedded nuclear, bar. Nevertheless, the scale ratio of the two peanuts in NGC 128 and especially in NGC 2549 (≈ 3 : 1) is rather low for a (large scale–i nuclear) bar configuration, and thus warrants further investigation.

In this paper we make use of a collisionless N–body simulation of a stellar disc evolving in isolation within a live dark matter halo, to study the development and stellar properties of a stable and persistent double (nested) configuration of X/peanut–shaped structures. In Section 2 we detail the simulation setup as well as the various secular processes it undergoes while evolving in isolation. In Section 3 we analyse mock–images generated from the simulation at an epoch where both nested peanuts have formed and stabilised, using a framework equivalently applicable to observational data. Here we model the radial surface density profile, and extract the parameters (size and strength) of the two nested X/P structures. In Section 4 we interpret and discuss the results, investigating the dynamics and formation of this nested configuration, and quantitatively comparing the X/P parameters with those of the CG16 sample. Section 5 concludes this study.

2 SIMULATION

We explore a purely collisionless N-body simulation of a multicomponent model for a galaxy consisting of three co-spatial disk populations: cold, warm, and hot disks represented by \( 10 \times 10^6, 6 \times 10^6, 4 \times 10^6 \) particles respectively. Such a setup is convenient for our analysis because each kinematic component has a different response to dynamical instabilities such as the vertical buckling instability of interest in this work (see Fragkoudi et al. 2017a). As such, the X/P development can be followed progressively and disentangled from other processes, as we shall detail further in the following Section. Further, a multiple-component disc additionally provides a more realistic configuration (e.g., Di Matteo et al. 2019), and reproduces observations Fragkoudi et al. (2018), thus rendering comparison with real galaxies all the more pertinent.

2.1 Simulation Set–up

Initially stellar particles are redistributed following a Miyamoto-Nagai density profile (Miyamoto & Nagai 1975) that has a characteristic scale length of \( b_{ini} = 4.7, 2.3, \) and 2.3 kpc, vertical thicknesses of 0.3, 0.6 and 0.9 kpc and masses of 2.5, 1.5, and \( 1.0 \times 10^{10} \) \( M_\odot \), respectively. Our simulation also includes a live dark matter halo (\( 5 \times 10^6 \) particles) whose density distribution follows a Plummer sphere (Plummer 1911), with a total mass of \( 1.6 \times 10^{11} \) \( M_\odot \) and a characteristic radius of 10 kpc. The stellar particles have a mass of \( 2.5 \times 10^{3} \) \( M_\odot \), while dark matter particles have a mass of \( 3.2 \times 10^{4} \) \( M_\odot \). For the N-body system integration, we used our parallel version of the TREE code with multi-thread usage under the AVX instructions. In the simulation we adopted the standard opening angle \( \theta = 0.5 \) and a gravitational softening parameter equal to 10 pc. For the time integration, we used a leapfrog integrator with a fixed step size of 0.1 Myr.

2.2 Evolution in Isolation

The galaxy is evolved for a total of 7 Gyr in isolation, during which time it undergoes a series of secular dynamical processes which give rise to the key structural components of interest in this study. By \( t \approx 5 \) Gyr the stellar bar is well in place and a double, nested X/peanut configuration has formed and begins to stabilise into a steady structure symmetric about the disc plane. The initial rotation curve is
shown in Figure 1 (left panel) and peaks at roughly 10 kpc, beyond which it displays a steady shallow decline. Overplotted in the same panel is the rotation curve at $t = 4.88$ Gyr, which shows a much steeper inner ascent, a broader peak and a slightly steeper decline compared to the initial conditions. The middle panel displays the disc’s gravitational stability to fragmenting, as expressed through the Toomre $Q$ parameter calculated as a function of radius, initially, and at $t = 4.88$ Gyr as before. Finally, as the disc evolves it transfers steadily angular momentum to the live halo, as shown in the right panel of Figure 1. This is rather typical, and by $t = 6.45$ Gyr the halo takes away roughly 13% of the disc’s angular momentum, essentially entirely from the vertical component $L_z$ (i.e., the rotation).

Figure 2 displays separately the 3 kinematical components of the simulation after $t = 6.45$ Gyr. In particular, the face-on view of the cold component -- which is the most sensitive to dynamical instabilities and perturbations (see e.g., Fragkoudi et al. 2017a) reveals that the disc has formed multiple spiral arms outside ~10 kpc, while within this radius there is a clear “thick” bar which has a lozenge or box-like shape, with a radius of roughly 6 kpc.

Beyond this radius, a thinner and dimmer bar extends outwards to approximately 10 kpc, and ends in anseae, or bar “handles” as they are sometimes referred to. These features are symmetric density enhancements at the ends of the bar, quite common in old, evolved systems like barred lenticulars (Martinez-Valpuesta, Knapen & Buta 2007). While the anseae are still discernible in the intermediate kinematic component, they are mostly “washed out” in the hot component, which retains the “thick” bar as the only distinctive structure apart from the disc. This progressive sensitivity to dynamical instabilities, from thin to thick components, will prove useful in disentangling the complicated structure of the bar in this simulation, and its associated X/P structures, as we detail in the following.

### 3 ANALYSIS

In this Section we dissect the simulation snapshot 145 corresponding to 6.45 Gyrs of evolution from the initial conditions, an epoch chosen such that the double X/P configuration of interest is well in place and stable. Mock-images were generated by projecting the simulation particles in the $(x-y)$ plane (disc viewed face-on) and $(R-z)$ plane (disc viewed edge-on), with $R$ being the radial co-ordinate along the direction of the bar’s major axis. This was done for all stellar particles as well as in detail for each kinematic component displayed Figure 2.

The edge-on view of this galaxy, as seen in the top panels of Figure 2, reveals the presence of a significant X-shaped structure extending out to, and indeed reaching a maximum at, a radius just under ~10 kpc. This is somewhat surprising, for two reasons. Firstly, this scale corresponds to roughly the end of the “thin” bar we see in the face-on view, whereas most of the studies to date find that it is only the inner half of bars which become unstable, and buckle to form a peanut (Lütticke, Dettmar & Pohlen 2000a, Skokos, Patsis & Athanassoula 2002a, Patsis, Skokos & Athanassoula 2002b, Laurikainen & Salo 2017, Erwin & Debattista 2017). Secondly, this scale coincides with the location of the anseae, which are generally believed to be confined to the disc plane. Apart from this apparent X-shaped structure, one can just discern a similar (though shorter) feature nested within. This inner peanut extends out to a radius just inside ~4 kpc, and also appears to be more boxy/peanut in shape, as opposed to the larger structure, which is rather strongly X-shaped. In the following we identify and quantify in detail the structural constituents of this simulated galaxy, separately for each disc component as well as their cumulative surface density distribution.

#### 3.1 Analysis of the Surface Density Distribution

##### 3.1.1 Structural Decomposition

We proceeded to analyse the mock-images described before as though they were real observations. The goal always being to perform a direct comparison between the simulation and galaxy observations, with the same methods and tools, we started by investigating the surface density distribution in these mock-images, mirroring the analysis of surface brightness distributions of galaxies in astronomical images. In the latter case, the radial surface brightness profile is routinely extracted, by fitting the galaxy isophotes as a function of photocentric distance, and further decomposed into its structural constituents (disc, bulge, bar, etc.). Here we extracted the radial surface density profile from the simula-
Figure 2. The three kinematic components after 6.45 Gyr: cold/thin (left), warm/intermediate (middle) and hot/thick (right). Top panels represent and edge-on view with the bar aligned such that it is side-on, while bottom panels represent the face-on view. The “outer” peanut reaches its maximum vertical extent at roughly the location of the ansae, as seen in the cold and intermediate components.

Figure 3. Structural decomposition of the surface brightness profile as observed in the simulation after 6.45 Gyr, in face-on orientation. Top: The best-fit decomposition consisting of an exponential disc (blue), a Gaussian ring (cyan), and three Sérsic components representing the pseudobulge (inner-most, red), and the two ‘nested’ bars (orange). Middle: Residual profile (data minus model). Bottom: Radial $B_0$ profile showing a ‘dip’ after $\sim$ 10 kpc, indicating the presence of ansae at that scale (Saha, Graham & Rodríguez-Herranz 2018).

Table 1. Decomposition Parameters

| Compt. (fn.) | $\mu_0/\mu_e$ | $h/R_e/R_{ansa}$ | $W_{ansa}^{(b)}$ | $n$ |
|--------------|---------------|-----------------|-----------------|-----|
| Disc [E]     | 8.94          | 4.88            | –               | –   |
| Ansa [G]     | 10.35         | 7.89            | 2.59            | –   |
| Thin bar [S] | 9.76          | 4.26            | –               | 0.11|
| Thick bar [S]| 8.01          | 2.13            | –               | 0.40|
| Pseudobulge  | 7.41          | 0.79            | –               | 0.56|

(a) – analytical function used to model the component: E = exponential; G = Gaussian; S = Sérsic
(b) – full width at half-maximum of the Gaussian component

We employed the software ISOFIT\footnote{https://github.com/BogdanCiambur/ISOFIT} (Ciambur 2015) to fit quasi-elliptical iso-density contours, as a function of distance (semi-major axis) from the centre, onto the mock-image oriented in face-on view.

A structural decomposition of the resulting one-dimensional surface density profile was performed with the software PROFILER\footnote{https://github.com/BogdanCiambur/PROFILER/} (Ciambur 2016), and the resulting best-fit model is shown in the top panel of Figure 3. The outer profile is dominated by the disc, which was modelled with an exponential. At a scale of 9 kpc, an excess from this exponential becomes apparent, and corresponds to the ansae. This was modelled with a Gaussian, which is the common parametric function employed to fit rings. Interior to this, the thin and thick bars were each modelled with Sérsic functions with indices ($n$) less than 1. Finally, a final excess becomes apparent in the central kpc, which is the pseudobulge that has developed from this galaxy’s secular evolution. This was also modelled with a Sérsic function. The parameters of the best-fit solution are shown in Table 1. The measured disc scale length at this epoch shows insignificant (less than 5%) evolution from the initial conditions, specifically compared to the thin disc $h_{ini} = 4.7$ kpc, which dominates the outer profile. As a cautionary note, these best-fit parameters of course correspond to the azimuthally-averaged 1D profile along a single direction, that of the major axis of the iso-density contours, i.e., approximately along the major axis of...
the bar (although the ellipse position angle was allowed to vary with radius). Although a simulation has the advantage of providing a complete 3D view of the galaxy, we again stress that the intention is to perform a one-to-one comparison of its structural properties with those in real galaxies, i.e., derived with the same method (that employed in CG16) in both cases.

The bottom panel in Figure 3 shows the radial $B_6$ profile as extracted in the face-on view. While the edge-on orientation is of interest for computing the X/P parameters, it is worth noting that even in face-on view, the $B_6$ signal is positive and significant along the length of the bar components, which implies that the morphology remains boxy/X-shape at all inclinations. Although multiple studies have shown that, in general, buckled bars display X/P isophotes at high disc inclination, they gradually assume the morphology of a “barlens” (Laurikainen et al. 2011, Athanassoula et al. 2015, Salo & Laurikainen 2017) as they approach face-on view. Nevertheless, Saha, Graham & Rodríguez-Herranz (2018) have shown through collisionless simulations that a 3-dimensional peanut morphology can indeed develop, supporting the earlier orbital analysis work of Patsis & Katsanikas (2014), who show that orbits supporting sharp X-like features located at energies beyond the ILR (non-periodic) might have a double-boxy nature, i.e., both in face-on and side-on views. Indeed, recently Smirnov & Sotnikova (2018) have shown that the presence of a bulge component, higher parent disc thickness, or higher Toomre Q parameter, are all factors which determine a barlens morphology in-plane. Consistent with these studies, our bulge-less simulation displays a 3D peanut, albeit with a weaker X/P signature in face-on view – where isophotes appear rather boxy, than that in edge-on projection – where the isophotes appear strongly X/peanut-shaped. The face-on $B_6$ profile suddenly turns negative at, and just after, the scale of the ansae, a behaviour additionally noted in Saha, Graham & Rodríguez-Herranz (2018) and interpreted as a tell-tale sign of the presence ansae.

The surface density profile thus indicates the presence of an inner, thick bar, as well as a longer and thinner bar component. This is not uncommon, and indeed shows similarities with the light profiles of NGC 2549 and, to a lesser extent, NGC 128, the two galaxies found to show a double peanut signature in CG16. We refer the reader to Figs. 4 and 9 in their paper, for comparison. Furthermore, the short, thick bar, and longer, thinner bar evident in this simulation may constitute a configuration similar to the Milky Way (Martínez-Valpuesta & Gerhard 2011). The presence of a long thin bar, in addition to the classical bar of our Galaxy, was noted by Hammersley et al. (1994), based on star counts in the Galactic plane. Further studies employing more refined tracers (Red Clump giants) have since confirmed its presence, and led to a series of papers where it is debated whether this long component is coupled to, or is misaligned with, the “classical bar” or “triaxial bulge” as it is sometimes referred to (Hammersley et al. 2000, López-Corredoira et al. 1999, 2007, Cabrera-Lavers et al. 2008, Wegg, Gerhard & Portail 2015).

3.1.2 Quantifying the X/Peanut Structures

Apart from the surface brightness profile along the major axis of the quasi-ellipses, ISOFIT also provides the geometric parameters of the iso-density contours, namely their position angle, ellipticity, and deviations from pure ellipses. These deviations are important, as they contain physical information pertaining to the different structures that make up the galaxy. Briefly, they are calculated by first fitting a pure ellipse on the mock image, at a given radius from the centre, and then performing a Fourier expansion along the ellipse, such that

$$\rho(\psi) = \rho_0 + \sum_{n} [A_n\sin(n\psi) + B_n\cos(n\psi)],$$  \hspace{1cm} (1)

where $\rho_0$ is the best-fit “average” surface density of the pure ellipse, $\psi$ is the eccentric anomaly angle which defines a point on this ellipse, $\rho(\psi)$ is the surface density at that point, while $n$ and $A_n, B_n$ are the order and coefficients of the different Fourier harmonics in the expansion. We refer the reader to (Ciambrug 2015) for further details. In the past, the $B_4$ harmonic has been used extensively to quantify the “boxyness” or “discyness” of galaxy isophotes, and correlating it with the galaxy’s physical properties (e.g., Davies et al. 1983; Bender 1988; Nieto, Bender & Surma 1991; etc.). More recently, CG16 have shown that the $B_6$ harmonic can serve as a robust tracer of X/peanut structures, and can serve to obtain quantitative parameters such as the length, height above the disc plane, and integrated “strength” of the instability. The $B_6$ was used for this purpose to study the geometry of the Milky Way’s own X/peanut-shaped structure and bar (Ciambrug, Graham & Bland-Hawthorn 2017). Further, Saha, Graham & Rodríguez-Herranz (2018) have applied this method to study the face-on view of X/P structures in simulations. In this work, the radial $B_6$ profile will serve as the primary tracer of the X/P feature.

To keep equivalence with the observational sample of CG16, we extracted the radial $B_6$ profile from the mock-images corresponding to projections of the simulation particles where the disc is viewed edge-on. In addition, the bar

![Figure 4. The X/P signature as measured in the 3 different kinematic components, as well as their superposition. (Cold component dominates the total signal, hot component is offset radially.)](image-url)
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ponent in Figure 3, which peaks at the ansae signature in the density profile (the Gaussian component in Figure 2. This scale additionally coincides with the large-scale X-shape structure clearly discernible in this figure that the total signal, plotted as the thick black line, was extracted for each disc component individually, as well as cumulatively from the superposition of the 3 components. The result is shown in Figure 4. It is immediately apparent as the full set of parameters is presented in Table 2.

Table 2. The X/P Diagnostics

|                  | \(\Pi_{\text{max}}\) | \(R_{\text{int}}\) | \(z_{\text{int}}\) | \(\psi\) |
|------------------|----------------------|-------------------|-------------------|---------|
|                  | [kpc, units of \(h\)] | [kpc, units of \(h\)] | [kpc, units of \(h\)] | [\({}^\circ\)] |
| In/thin          | 0.056±0.010          | 4.27±0.82         | —                 | —       |
| In/intern.       | 0.060±0.006          | 4.14±0.82         | —                 | —       |
| In/thick         | 0.035±0.003          | 2.75±0.82         | —                 | —       |
| **In/total**     | 0.050±0.006          | 3.94±0.21, 0.89±0.11 | 1.45±0.21, 0.33±0.11 | 5.15±2.21, 1.17±0.50 | 1.49±0.29, 0.34±0.09 | 20 |
| Out/thin         | too noisy            | —                 | —                 | —       |
| Out/intern.      | 0.082±0.009          | 8.03±0.82         | —                 | —       |
| Out/thick        | 0.053±0.005          | 6.09±0.82         | —                 | —       |
| **Out/total**    | 0.122±0.012          | 8.33±0.22, 1.88±0.21 | 2.44±0.21, 0.55±0.20 | —       |

(a)– maximum amplitude of \(B_6\) harmonic; (b)– intrinsic radius of X/P structure; (c)– intrinsic vertical height of X/P structure; (d)– integrated strength of the \(B_6\) profile; (e)– full width at half-maximum of the \(B_6\) profile; (f)– angle of the “X” arm relative to the major axis.

was also rotated such that it is viewed side-on. The \(B_6\) profile, as the thick black curve, shows a prominent peak at roughly 8 kpc, which corresponds to the large-scale X-shape structure clearly discernible in Figure 2. This scale additionally coincides with the ansae signature in the density profile (the Gaussian component in Figure 3, which peaks at \(R_\text{ansa} = 7.89\) kpc). The second feature of note is a second, intermediate–strength peak at an interior radius, of \(\approx 4\) kpc. This corresponds to the smaller, more peanut-shaped feature nested within the large-scale X. When we dissect the total signal by kinematic components, we find, unsurprisingly, that the thin component dominates the outer X/P signature, and also shows a strong signal for the inner peanut. The intermediate component is comparable in amplitude at 4 kpc, but sub-dominant (though still significant), for the outer X. Finally, the hot component also appears to show two significant peaks, less prominent than in the colder components, and offset towards the centre with respect to the intermediate and the cold components’ \(B_6\) signatures. Interestingly, we note a third peak in the \(B_6\) profile occurring at \(R_\text{int} \approx 0.6\) kpc in the cold and warm components, and just beyond 1 kpc in the hot disc, where it is not clearly separated from the other peaks at larger radii. This could indicate the presence of a third peanut structure, possibly associated with a decoupled nuclear bar. Indeed, the beat feature which appears in the main bar’s strength (\(A_2\)) and pattern speed evolution, as shown in Figure 5, could result from its interference with such a nuclear bar. This third inner X/P feature tentatively shows up in the face-on density projections as well, but occurs on a scale too small for a fully reliable measurement. Hence, we do not include this feature in our analysis.

As per CG16, we compute the different parameters of the X/P structures, including the intrinsic radius (\(R_{\text{int}}\)), the height above the disc plane (\(z_{\text{int}}\)), the integrated “strength” (\(S_\text{int}\)), starting from the \(B_6\) profile. Briefly, these correspond to the radial scales where \(B_6\) reaches a maximum for the former two, while the latter is defined as the FWHM around the peak. The full set of parameters is presented in Table 2.

3 NB: This location does not necessarily correspond to the “end” of the peanut, as the \(B_6\) usually falls-off more or less gradually from the maximum point. Hence, a weaker X/P signature remains, and trails off, beyond the \(B_6\) peak location.

3.2 A Few Notes on the Dynamics

Before attempting to interpret the double X/P configuration, there are a number of aspects that are worth pointing out. First, the fact that the outer X overlaps the face-on ansae appears surprising, since the latter are canonically believed to accumulate around the co-rotation radius, where vertical instabilities are minimal. However, this is a relatively slow bar, rotating with a pattern speed of \(\Omega_p \approx 9\) km/s/kpc (see Figure 5), which places the co-rotation radius beyond 20 kpc, almost twice the scale of these ansae. Skokos, Patsis & Athanassoula (2002b) have studied the parameter space of buckling bars, including the bar pattern speed, and
In the top panel of Figure 6 we display the angular velocity diagram calculated from the simulation snapshot of interest. In Figure 1, which may prevent the bar to extend beyond that radius and possibly entrain the formation of the ansae as well as confine the outer X-shaped structure. Indeed, the galaxy rotation curve has been shown to affect the 3D morphology of X/P structures (Salo & Laurikainen 2017). A similar example, of stellar overdensities to the point where it begins to settle into the double X/P configuration (t ≈ 4.75 Gyr).

We observe the buckling instability develop, characterised by vertically asymmetric bending modes (“smile – frown”, or “banana” orbits), and rather strong within 3 – 3.5 Gyr. This phase occurs mostly interior to 5 kpc, or roughly half the radius of the bar. By 3.5 Gyr we begin to notice 2 components in this thick part of the bar, namely a peanut-shaped component and an X-shaped feature over-lapping it, and slightly more extended in radius. During the subsequent evolution, the peanut-shaped structure undergoes very little change, and ends up as the inner peanut, whereas the X extends in radius and undergoes further buckling perpendicular to the disc plane. This component ends up as the strong outer X structure, peaking in strength at ~ 8 kpc for the thin and intermediate components, respectively, and ~ 6 kpc for the thick component (see Table 2).

By the epoch chosen for the analysis above (6.25 Gyr) the peanut-shaped structure undergoes very little change, and ends up as the inner peanut, whereas the X–shaped component and an X-shaped feature over-lapping it, and slightly more extended in radius. During the subsequent evolution, the peanut-shaped structure undergoes very little change, and ends up as the inner peanut, whereas the X extends in radius and undergoes further buckling perpendicular to the disc plane. This component ends up as the strong outer X structure, peaking in strength at ~ 8 and ~ 7 kpc for the thin and intermediate components, respectively, and ~ 6 kpc for the thick component (see Table 2). The double X/P configuration is well stabilised.

Throughout their evolutionary course, the two components retain their dynamical coupling, both rotating with
the same pattern speed. They are thus clearly different manifestations occurring in the same stellar component, and therefore likely supported by different orbit families. Qualitatively, the setup appears to be a superposition of the two morphological classes of boxy/peanut/X -shaped structures defined by Bureau et al. (2006), namely “CX” and “OX”, the first being features whose four X “arms” cross the photo-centre (×), while the second exhibiting arms which cross the disc plane but do not meet in the centre (> <). By studying the orbital dynamics around the vertical ILR region, Patsis & Harsoula (2018) have shown how a broad variety of X/Peanut morphologies can be supported through various combinations of stable 3D periodic orbits, and quasi-periodic or chaotic orbits trapped around them which can support either a CX or OX morphology. In particular, the general morphology of the outer “X” in our case – bow-tie shaped, with a well defined and abrupt end – is reminiscent of the OX configuration obtained in Patsis & Harsoula (2018) via sticky-chaotic, or quasi-periodic orbits at different energies (their Figs. 5c and 7). The latter findings are indeed supported by Smirnov & Sotnikova (2018) and Parul, Smirnov & Sotnikova (2020), who note the presence of double–X features in their simulation for certain initial conditions (in terms of Toomre Q and disc scale height), where a secondary bar buckling eventually settles into a stable double X-like configuration. It is possible that factors such as the absence of a significant classical bulge component to stabilise the inner bar, and the latter’s relatively low pattern speed (cf. Skokos, Patsis & Athanassoula 2002b), play a role in facilitating the population of the different orbit families which end up supporting the two nested structures.

4.2 Comparison with Nearby Galaxies

CG16 have studied the structural parameters of X/P structures in 12 edge-on galaxies known in the literature to host such features. They have shown that some of the peanut parameters – as measured analogously here, in Section 3.1.2 – are correlated, roughly defining a number of scaling relations. These provide a useful benchmark to compare our sim-
Figure 9. NGC 2549, an edge-on galaxy with a double X/P configuration, as observed with SDSS in the $r$ band (left), and at higher resolution with HST, at 702 nm (right). Unlike the simulation analysed in this paper, here the inner peanut structure appears to be stronger, with a well defined bow-tie, or ‘X’ shape, while the larger scale structure is weaker. The two X/P structures are well separated, as shown by their extracted $B_6$ profile (see Ciambur & Graham 2016, Figure A1 in their Appendix.)

Figure 10. The vertical size ($z_{\Pi,\text{max}}$) of the X/P structure as a function of its projected radial extent, $R_{\Pi,\text{max}} \sin(\delta)$. Solid circles correspond to the observational sample in Ciambur & Graham 2016, the star symbol corresponds to the Milky Way (with intrinsic, not projected, $R_{\Pi,\text{max}}$), while the green squares correspond to the 3 peaks in the $B_6$ profile of this simulation. Quite clearly larger than the sample average, notably in radius, both the inner and outer X/P structures lie on the general trend nevertheless.

The size of X/P structures is also related to their integrated strength, as shown in Figure 11. In order to exclude the effect of variation in galaxy size, this relation was additionally normalised by disc size (i.e., the exponential scale length $h$). The relation still holds, indicating the tight connection between X/P structures and the host discs they

4 Unusually small for a large-scale bar plus embedded nuclear bar configuration.
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originates from. Here we employed the measured value of $h = 4.88$ kpc for full consistency with the observational approach. Once again it is apparent that the inner peanut in the simulation falls on the expected trend, whereas the outer X is significantly stronger than expected, in particular in the $(z_{\Pi,\text{max}} - S_{\Pi})$ plane. That is, it is a strong and longer than usual X-shaped structure, indeed extending all the way to the end of the bar, but which nonetheless remains relatively confined in the vertical direction. This is confirmed by the small opening angle of its X arms (Table 2). We note that in Figure 11 the two data points corresponding to the outer X feature are the measurements on the thick and intermediate components, as the thin component was too noisy for a reliable measurement, and consequently the total image as well, as it is dominated by the latter component. As such, although strong, the two data points are lower limits of the total $S_{\Pi}$ of the outer X structure.

Comparing this simulation with nearby galaxies leads to conclude that the inner X/P feature is indeed a rather typical peanut, consistent with the theoretical formation scenarios, as well as with sizes (including fraction of the host bar size) and strengths of observed galaxies. Conversely, the outer structure is significantly stronger, sharper and has a X or “bow-tie”, rather than peanut, morphology. Both its strength and size make it an outlier of the structural scaling relations defined by the CG16 sample, and the fact its maximal vertical extent edge-on corresponds roughly to the end of the bar (the scale of the face-on ansae) seems unusual. Nevertheless, this radial scale is also the location of the vILR, where a boxy/peanut feature is indeed expected to reach its maximal height (Combes et al. 1990). Canonnically, peanut structures are observed to arise as a thickening of roughly the inner half of bars ($\approx 0.4 - 0.5 R_{\text{bar}}$; Lütticke, Dettmar & Pohlen 2000b, Laurikainen & Salo 2017, Erwin & Debattista 2017). It is therefore important to understand the formation and physical relevance of such extended X structures in N-body simulations which aim to explain and constrain the secular evolution of barred galaxies, as well as the Milky Way (e.g., Di Matteo et al. 2015, Debattista et al. 2017, Fragkoudi et al. 2017b, Di Matteo et al. 2019). We reserve such an investigation for future works.

5 CONCLUSIONS

In this paper we study a pure N-body simulation of a barred disc galaxy, consisting of a stellar disc embedded in a live dark matter halo, which develops two co-existing X/peanut-shaped structures, in a nested configuration, which form after $\approx 3.5$ Gyr, and stabilise after $\approx 5$ Gyr of evolution in isolation. The simulation initially consists of a pure disc made up of three kinematic components – thin, intermediate, and thick. The absence of a classical bulge component facilitates the identification and quantification of the components of interest, particularly in the central region, where bulges otherwise dominate the light distribution in all but the later-type spiral galaxies.

We extract and model the face-on major axis surface density profile from mock-images constructed from the simulation, analogously to a photometric decomposition of a galaxy image. We further extract the edge-on radial $B_{\rho}$ profile, which captures the signature of the two nested X/peanut-shaped structures, and use it to quantify their radial and vertical extents ($R_{\Pi}$, $z_{\Pi}$), as well as their respective

\[ R_{\Pi}, \text{max} \times [\text{kpc}] \]

\[ 0.5 \leq R_{\Pi}, \text{max} \leq 2.5 \]

\[ z_{\Pi}, \text{max} \times [\text{kpc}] \]

\[ 0.0 \leq z_{\Pi}, \text{max} \leq 1.0 \]

\[ S_{\Pi} \times [\text{units of } h] \]

\[ 0 \leq S_{\Pi} \leq 0.5 \]

\[ R_{\Pi}, \text{max} \times [\text{units of } h] \]

\[ 0.0 \leq R_{\Pi}, \text{max} \leq 2.5 \]

\[ z_{\Pi}, \text{max} \times [\text{units of } h] \]

\[ 0.0 \leq z_{\Pi}, \text{max} \leq 1.0 \]

\[ S_{\Pi} \times [\text{units of } h] \]

\[ 0 \leq S_{\Pi} \leq 0.5 \]

\[ R_{\Pi}, \text{max} \times [\text{units of } h] \]

\[ 0.0 \leq R_{\Pi}, \text{max} \leq 2.5 \]

\[ z_{\Pi}, \text{max} \times [\text{units of } h] \]

\[ 0.0 \leq z_{\Pi}, \text{max} \leq 1.0 \]

\[ S_{\Pi} \times [\text{units of } h] \]

\[ 0 \leq S_{\Pi} \leq 0.5 \]

\[ R_{\Pi}, \text{max} \times [\text{units of } h] \]

\[ 0.0 \leq R_{\Pi}, \text{max} \leq 2.5 \]

\[ z_{\Pi}, \text{max} \times [\text{units of } h] \]

\[ 0.0 \leq z_{\Pi}, \text{max} \leq 1.0 \]

\[ S_{\Pi} \times [\text{units of } h] \]

\[ 0 \leq S_{\Pi} \leq 0.5 \]

\[ R_{\Pi}, \text{max} \times [\text{units of } h] \]

\[ 0.0 \leq R_{\Pi}, \text{max} \leq 2.5 \]

\[ z_{\Pi}, \text{max} \times [\text{units of } h] \]

\[ 0.0 \leq z_{\Pi}, \text{max} \leq 1.0 \]

\[ S_{\Pi} \times [\text{units of } h] \]

\[ 0 \leq S_{\Pi} \leq 0.5 \]

\[ R_{\Pi}, \text{max} \times [\text{units of } h] \]

\[ 0.0 \leq R_{\Pi}, \text{max} \leq 2.5 \]

\[ z_{\Pi}, \text{max} \times [\text{units of } h] \]

\[ 0.0 \leq z_{\Pi}, \text{max} \leq 1.0 \]

\[ S_{\Pi} \times [\text{units of } h] \]

\[ 0 \leq S_{\Pi} \leq 0.5 \]

\[ R_{\Pi}, \text{max} \times [\text{units of } h] \]

\[ 0.0 \leq R_{\Pi}, \text{max} \leq 2.5 \]

\[ z_{\Pi}, \text{max} \times [\text{units of } h] \]

\[ 0.0 \leq z_{\Pi}, \text{max} \leq 1.0 \]

\[ S_{\Pi} \times [\text{units of } h] \]

\[ 0 \leq S_{\Pi} \leq 0.5 \]
tive integrated strength ($S_1$). The main conclusions are as follows:

- The two X/P features are not associated with two distinct bars, but remain dynamically coupled throughout, rotating with the bar’s pattern speed of $\Omega_p \approx 9 \text{ km/s/kpc}$ at $t = 6.45$ Gyr, a time where the configuration is in place, stable and symmetric. This is a rather slow bar, which only extends out to roughly half the radius of co-rotation.
- The inner, ‘classical’ peanut-shaped structure develops following a vertical buckling instability of the bar. It peaks at $R = 3.94 \pm 0.21$ kpc, roughly half the radius of the bar, and its size and strength is consistent with those found in external galaxies.
- The outer structure is considerably stronger, distinctly X- or (bow-tie)-shaped, and peaks at $R = 8.33 \pm 0.22$ kpc, a scale roughly coinciding with the end of the bar and the scale of the latter’s ‘handles’, or ansae. While the vertical extent is not significantly higher than expected, the radius and strength make it an outlier of the trends seen in nearby galaxies. This feature develops shortly after the inner peanut, and gradually extends in radius, over the span of $\sim 1.5$ Gyr, from $\sim 5$ kpc to its final stable radius just over 8 kpc, all while showing little change in its vertical size.

We conclude that the two nested peanuts likely arise from inherently different dynamical mechanisms, appearing to be a superposition of the CX and OX morphological classes. Multiple X/P morphologies can be supported via various combinations of periodic, quasi-periodic, or chaotic orbits, as recently shown by Patsis & Harsoula (2018) and Parul, Smirnov & Sotnikova (2020), and the absence of a classical bulge component to stabilise the slow bar in our simulation might facilitate the population of families that support a long-lasting double configuration. A detailed orbit frequency analysis is required to constrain the specific orbital backbones of the two structures, which however goes beyond the scope of this paper and we reserve for future work.

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