Feedback Linearization Control Design for Battery/SMES Hybrid Energy Storage Systems Used in Distribution Network

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A battery/superconducting magnetic energy storage (SMES) hybrid energy storage system (BSM-HESS) is designed for a power system. Meanwhile, a nonlinear feedback control (FLC) is adopted to achieve smooth and fast-tracking performance, and a rule-based strategy (RBS) is applied for power demand allocation. FLC can effectively compensate for the system’s nonlinearity to obtain the global consistent control performance; thus, it can properly solve the nonlinearity and modeling uncertainty of BSM-HESS. The effectiveness and advantages of FLC are evaluated via three cases, namely, heavy load condition, light load condition, and robustness with uncertain BSM-HESS parameters. Simulation results show that compared with proportional–integral–derivative (PID) control, FLC can achieve the best dynamic performance under various working conditions, which is beneficial for the system to quickly restore stable operation after large disturbance. In addition, the control cost of FLC is lower than that of PID control under both heavy load and light load conditions.

Keywords: battery/SMES hybrid energy storage system, distribution network, feedback linearization control, rule-based strategy, parameter uncertainties

INTRODUCTION

In recent years, with large-scale and widespread integration of renewable energy into the power system, energy storage systems (ESSs) have become a hot research topic (Yang et al., 2015; Zhang et al., 2016; Bakeer et al., 2021). The energy storage system used in the power system refers to the device that can store a certain amount of electric energy and can quickly convey or absorb active and reactive power when abnormal events occur to the power system (Xi et al., 2016; ASV et al., 2020). In a transmission system, energy storage equipment is mostly installed on the transmission side of the line to improve the stability of system and rapid response speed (Zhang et al., 2015; Bakeer et al., 2021). In the distribution system, the energy storage device is usually equipped on the load side to protect the important load and balance frequency fluctuation (Nayak et al., 2021).

Electric energy storage has many forms that can mainly be divided into two types: energy storage and power storage (Chaibi et al., 2019; Li et al., 2019). Energy storage represented by lead-acid battery, lithium battery, and sodium-sulfur battery has high energy density and long energy storage time but the low power density and short cycle life (Luo et al., 2015; Ruan et al., 2019). Power-type energy storage represented by a super capacitor, flywheel energy storage, and superconducting magnetic energy storage (SMES) has the advantages of high power density, fast response speed, and long cycle life but with deficiencies of low energy density and high self-discharge rate (Adhikari and Li, 2014; Akyurek and Rosing, 2016; Zhang et al., 2021).
It is difficult for a single energy storage technology to have all the aforementioned advantages at the same time to meet the requirements of different application modes (Lalouni et al., 2009; Khalid and Savkin, 2010; Worthmann et al., 2015). However, based on technical complementarity of volumetric energy storage and power-type energy storage, hybrid energy storage can be used to meet the technical requirements of various levels. At present, battery/SMES hybrid energy storage systems (BSM-HESSs) that can effectively improve the stability and reliability of the system have received worldwide research interests (Dali et al., 2010; Malysz et al., 2014; Melo et al., 2019). As the core of the control system, the design of the control strategy plays the most critical role that has both important theoretical and practical significance.

BSM-HESS can effectively improve system stability, the performance of which is closely related to the selected control mode (Bazargan et al., 2018; Serir et al., 2016; Teymour et al., 2014). At present, research on control schemes is mostly focused on proportional–integral–derivative (PID) control (Brenna et al., 2016). However, this method needs to establish an accurate mathematical system model and often focuses on the design of a certain operation point. When the operation point of system changes, the performance will be dramatically affected, and the robustness is poor (Hussain et al., 2017). In order to remedy the existing deficiencies, a large number of academic nonlinear control theories are developed. Magdy et al. (2018) have proposed a coordination of load frequency control (LFC) and SMES technology using a new optimal PID controller–based moth swarm algorithm in the Egyptian power system while considering high wind power penetration. Besides, a new adaptive control strategy based on the particle swarm optimization algorithm is proposed for the optimization of control strategy for a hybrid electric vehicle energy storage system (Ye et al., 2020). Meanwhile, Lin and Lei (2017) have developed a hierarchical control strategy for a hybrid energy storage system. However, the aforementioned studies all have the characteristics of a complex structure, low implementation feasibility, and weak adaptability; thus, their control design needs to be further improved.

Over the last decade, research on the feedback linearization–based nonlinear control theory has achieved great progress, which can successfully transform nonlinear systems into linear systems through state feedback in coordinate transformation domain. Direct feedback linearization is a representative feedback linearization method based on input and output descriptions of the system, which has been utilized to solve many control problems of nonlinear systems. Therefore, a feedback linearization control (FLC) for BSM-HESS is proposed in this article, to realize an efficient and smooth tracking.

The remaining of this article is organized as follows: Battery/SMES Hybrid Energy Storage Systems Modeling introduces the BSM-HESS model. In FLC Design for BSM-HESS, FLC design is described. Case studies are carried out in Case Studies section, along with simulation results analysis. At last, Conclusion summarizes the main contributions of the study.

**BATTERY/SMES HYBRID ENERGY STORAGE SYSTEMS MODELING**

Distributed generation (DG) owns the merits of easy installation, pollution-free, and low costs. As a backup power source of the power system (Huang et al., 2021; Sai et al., 2021), it can ensure the stability and reliability of user’s electricity consumption. Although distributed energy has many advantages, there are still many shortcomings; for instance, the control mode of DG is very complex, and the access cost is high (Bizon, 2018; Shi et al., 2018). In addition, since DG is an uncontrollable source, it is imperative to solve the limitations and isolation problems of DG to reduce the influence of DG on large power grid (Murtty and Kumar, 2021). In general, DG is a micro-generation unit that can realize energy conversion and independent control. Compared to a distribution network, DG can be regarded as a controlled unit, such that the difficulty of configuring the capacity of DG can be greatly reduced. Microgrids are vulnerable to internal distributed power supply and load fluctuations due to capacity and scale limitations, and ESS provides solutions for these problems. At present, it is difficult for a single energy storage device to simultaneously achieve multiple functions such as power quality improvement and microgrid stability control, so different energy storage devices need to be coupled together for use (Ali et al., 2010; Kasilingam and Pasupuleti, 2015; Olujobi, 2020).

The combination of battery and SMES takes both the instantaneous power supply advantages of SMES and the long-term power supply capacity of battery into account, which specifies the excellent power supply characteristic of BSM-HESS. Besides, BSM-HESS has another advantage compatible with both, such as high energy density and high power density, which surpasses the effect of either (Jae Woong Shim et al., 2013; Kouchachvili et al., 2018). The charging and discharging models of key components of BSM-HESS, that is, battery and SMES, are presented in *Figure 1*.

**FLC Design for Storage Systems**
where duty cycles $D_1$ and $D_2$ are restricted in a subset of $(0, 1)$ for the purpose of ensuring operation safety and efficiency. The meanings of other symbols can be referred to Nomenclature.

**FLC DESIGN FOR BSM-HESS**

**Rule-Based Strategy**
The rule-based strategy (RBS), also called logical threshold control strategies, is widely used in engineering practice due to their simplicity and practicality. Heuristic rules or fuzzy logic rules are used to determine the control variable output according to preset conditions. It mainly includes state machine control, threshold control, and power tracking control to ensure the main components work in the most efficient area.

The load power $P_{\text{demand}}$ is the prerequisite of the determination of a qualified EMS, where the power distribution between SMES and battery is optimized. The application constraints of BSM-HESS based on RBS are as follows:

(a) State of charge (SOC) of SMES:

\[
\frac{i_c}{i_{c,\text{max}}} \geq \frac{1}{2},
\]

where $i_c$ and $i_{c,\text{max}}$ denote the current value and maximum allowable current value of the SMES, respectively. When the constraint is not satisfied, SMES will be charged by the battery with a constant power $P_{ch}$.

(b) SOC of battery:

\[
0.2 \leq \frac{Q_c}{Q_l} \leq 0.9,
\]

where $Q_c$ and $Q_l$ are the total charge of the battery and the remaining charge of the battery, respectively.
(c) Constraints of $P_{\text{demand}}$:

When $P_{\text{demand}} \geq 0$ is satisfied, the constraints are as follows:

$$
\begin{align*}
    P_{\text{demand}} &= P_{\text{demand}} + P_{\text{SMES}} = 0 (P_{\text{demand}} \leq P_{\text{min}}) \\
    P_{\text{min}} &= P_{\text{battery}}, P_{\text{SMES}} = P_{\text{demand}} - P_{\text{min}} (P_{\text{demand}} > P_{\text{min}}). 
\end{align*}
$$

(4)

The power threshold $P_{\text{min}}$ is set to ensure that once the power demand $P_{\text{demand}}$ is lower than the threshold, SMES will not supply power to the load.

When $P_{\text{demand}} < 0$ is satisfied, the regenerative energy is absorbed by SMES before the battery is fully charged, and the charging cycle is shortened, thus prolonging the battery life.

**Feedback Linearization Control Theory**

Feedback linearization is a typical approach in the nonlinear control theory. The idea is to transform a nonlinear system dynamic into an equivalent (fully or partly) linear one through a change of state variables and a suitable nonlinear control input, so that linear control techniques can be then applied to the nonlinear system.

Here, a standard affine multiple-input multiple-output system is considered in a neighborhood around an operation point $x_0$ of the form

$$
\begin{align*}
    \dot{x} &= f(x) + g(x)u \\
    y &= h(x),
\end{align*}
$$

(5)

where $x \in R^n$ is the state vector, $u \in R^m$ is the control input vector, $y \in R^m$ is the output vector, $f(x) \in R^n$, $g(x) \in R^{m \times m}$, and $h(x) \in R^m$ are smooth. The inputoutput linearization of a multiple input multiple output system is obtained via differentiating the output $y_i$ of the system until the input $u_i$ appears, assuming that $r_i$ is the smallest integer such that at least one of the inputs explicitly appears in $y_i^{(r_i)}$:

$$
y_i^{(r_i)} = L_i^T h_i \sum_{j=1}^{r_i} L_j L_j^T h_j u_j,
$$

(6)

where $y_i^{(r_i)}$ denotes the $i$th-order derivative of $y_i$, if $L_j L_j^T h_j(x) \neq 0$ for at least one $j$. For at least one $y_i$ gives

$$
\begin{align*}
    \begin{bmatrix}
    y_1^{(r_1)} \\
    \vdots \\
    y_i^{(r_i)} \\
    \vdots \\
    y_m^{(r_m)}
    \end{bmatrix} &= \begin{bmatrix}
    L_i^T h_i \\
    \vdots \\
    L_i^T h_i \\
    \vdots \\
    L_m^T h_m
    \end{bmatrix} + B(x) \begin{bmatrix}
    u_1 \\
    \vdots \\
    u_m
    \end{bmatrix}. 
\end{align*}
$$

(7)

$$
B(x) = \begin{bmatrix}
    L_{g_{11}} L_{f_{11}}^{-1} h_1 & \cdots & L_{g_{m1}} L_{f_{11}}^{-1} h_1 \\
    \vdots & \ddots & \vdots \\
    L_{g_{1m}} L_{f_{m1}}^{-1} h_m & \cdots & L_{g_{mm}} L_{f_{m1}}^{-1} h_m
    \end{bmatrix}. 
$$

(8)

Here, $B(x)$ is the $n \times m$ control gain matrix, if $B(x)$ is invertible, the physical control law of the multiple input multiple output nonlinear system can be derived as follows:

$$
\begin{align*}
    (u) &= B(x)^{-1} \begin{bmatrix} -L_i^T h_i \\
    \vdots \\
    -L_m^T h_m \\
    \vdots \\
    v_m 
    \end{bmatrix},
\end{align*}
$$

(9)

$$
(v_i) = - \sum_{j=1}^{r_i-1} \alpha_j y_j^{(i)}
$$

where $v_i$ is the new input of the system and $\alpha_j$ is the linear control gain.

**Underlying Controller Design**

For BSM-HESS (1), the state vector can be defined as $x = (x_1, x_2, x_3, x_4, x_5)^T = (v_1, v_2, i_1, i_2, v_o)^T$, output $y = (y_1, y_2)^T = (i_1, v_o)^T$, control input $u = (u_1, u_2)^T = (D_1, D_2)^T$, and tracking error $e = [e_1, e_2]^T = [v_1 - v_o, v_o - \hat{v}_o]^T$. Then, the tracking error $e$ is differentiated until the control input $u$ explicitly appeared as follows:

$$
\begin{align*}
    \dot{e}_1 &= \frac{v_1}{L_1} + \left(\frac{R_{m1} - R_{m2}}{L_1} D_1 - \frac{R_{m1} + R_{m2}}{L_1} D_1 - \frac{v_o}{L_1} - \hat{v}_o \right), \\
    \dot{e}_2 &= (1 - D_1) \frac{i_1}{C_o} + (1 - D_2) \frac{i_2}{C_o} - \frac{v_o}{R_C} - \hat{v}_o
    \end{align*}
$$

(10)
In addition, system 2) can be represented in the concise matrix form as follows:

\[
\begin{bmatrix}
\dot{y}_1 \\
\dot{y}_2
\end{bmatrix} = 
\begin{bmatrix}
g_1(x) \\
g_2(x)
\end{bmatrix} + B(x) \begin{bmatrix}
u_1 \\
u_2
\end{bmatrix} - \begin{bmatrix}
i_1^* \\
i_2^*
\end{bmatrix},
\]

(11)

where

\[
g_1(x) = \frac{v_1 - v_o}{L_1} - \left(\frac{R_{L1} + R_{on2}}{L_1}\right)i_1
\]

(12)

\[
g_2(x) = (1 - D_1) \frac{i_1}{C_o} - \frac{v_o}{R C_o} + \frac{i_2}{C_o}
\]

(13)

with

\[
B(x) = \begin{bmatrix}
b_{11} & 0 \\
0 & b_{22}
\end{bmatrix} = \begin{bmatrix}
\frac{R_{on2} - R_{on1} i_1 + v_o}{L_1} & 0 \\
0 & -\frac{i_2}{C_o}
\end{bmatrix}.
\]

(14)

To ensure the aforementioned input-output linearization to be valid, the control gain matrix \(B(x)\) must be nonsingular among the whole operation range, that is,

\[
\det[B(x)] = -\frac{i_2 [ (R_{on2} - R_{on1}) i_1 + v_o ]}{C_o L_1} \neq 0.
\]

(15)

Since SMES current \(i_2\) is always different from zero, for example, a value of zero means that SMES stops operating.

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**TABLE 1 | BSM-HESS parameters.**

| Symbol | Parameters | Value | Unit |
|--------|------------|-------|------|
| \(L_1\) | Battery side inductance | 680 | \(\mu\)H |
| \(R_0\) | Battery series resistance | 0.04 | \(\Omega\) |
| \(R_{L1}\) | Battery side inductor series resistance | 0.25 | \(\Omega\) |
| \(C_1\) | Battery side filter capacitance | 1 | mF |
| \(L_2\) | SMES side inductance | 39 | mH |
| \(R_{L2}\) | SMES side inductor series resistance | 0.114 | \(\Omega\) |
| \(C_2\) | SMES side filter capacitance | 0.22 | mH |
| \(L_{sc}\) | Superconducting magnetic coil inductance | 25 | H |
| \(R_{on}\) | MOSFET on-resistance | 0.021 | \(\Omega\) |
| \(C_0\) | Load side capacitance | 1 | mF |

**TABLE 2 | Controller parameters.**

| FLC | \(\lambda_1\) | 120 |
|-----|---------------|-----|
|     | \(\lambda_2\) | 150 |
| PID control | \(K_{p1}\) | 462 |
|     | \(K_{i1}\) | 328 |
|     | \(K_{d1}\) | 45 |
|     | \(K_{p2}\) | 425 |
|     | \(K_{i2}\) | 287 |
|     | \(K_{d2}\) | 42 |

**FIGURE 3 | Overall FLC structure for BSM-HESS.**
thus, the controllability of SMES is lost. Meanwhile, DC bus voltage \( v_o \neq (R_{on1} - R_{on2})i_1 \) is always valid among the whole operation range. Therefore, the aforementioned condition is always valid.

The final FLC strategy is designed as follows:

\[
\begin{bmatrix}
\dot{u}_1 \\
\dot{u}_2
\end{bmatrix} = B^{-1} \begin{bmatrix}
\frac{v_1 - v_o}{L_1} + \left( \frac{R_{L1} + R_{on2}}{L_1} \right)i_1 + i_1^* - \lambda_1 e_1 \\
\frac{v_1}{C_o} + \frac{v_o}{R_{C_o}} - \frac{i_2}{C_o} + v_o^* - \lambda_2 e_2
\end{bmatrix},
\]

(16)

where \( \lambda_1 \) and \( \lambda_2 \) are the control gains. In addition, the overall FLC structure of BSM-HESS is given in Figure 3.

**CASE STUDIES**

The parameters of BSM-HESS and controller are shown in Table 1 and Table 2, respectively. The initial SOC of the battery is set to 90%, the minimum voltage of the battery is 36 V, the maximum voltage is 144 V, and battery pack contains 48 LiFePO4 cells that are connected
in series. The rated current of SMES is 100A. In addition, in RBS, $P_{\text{min}} = 2\, \text{kW}$ and $P_{\text{ch}} = 100\, \text{W}$. Case studies are carried out by Matlab/Simulink 2019b. Besides, the sampling rate was set to $10^{-4}\, \text{s}$, and ode23 was selected as the solver.

**Heavy Load Condition**

Based on the BSM-HESS model, the continuous step change of power demand of the power system under various conditions is studied to validate the specific tracking performance under heavy load conditions. In practical engineering application, heavy load condition usually occurs when the power system is connected with a large load. Here, the regenerative braking is carried out under the condition of corresponding negative load power, while the DC bus voltage reference is maintained at 160 V. The detailed system responses are shown in Figure 4, which shows that FLC can smoothly track the change of power demand and stably maintain the DC bus voltage. Compared with PID control, FLC has the smallest tracking error and the highest tracking speed. It is worth noting that such smooth tracking ability is very crucial for economic and reliable power system operation and can considerably prolong the battery service life.

**Light Load Condition**

The aim of this case is to study the control performance of FLC when the power system is connected with a small load.

![BSM-HESS responses under light load conditions.](image)
At this time, another power demand step change is used to compare the tracking performance between FLC and PID control. The corresponding responses are shown in Figure 5. It can be found that FLC achieves better tracking performance in terms of tracking speed and tracking error than PID control. In addition, FLC has smoother regulation of power $P$, while PID control oscillates severely. Similarly, for DC bus voltage, FLC has a small overshoot and can restore the disturbed power system in a short period of time, while PID control requires much more time for disturbed power system restoration with larger overshoot. Therefore, FLC can effectively decrease the charge and discharge frequency of the hybrid energy storage system, to reduce the wear and tear of the hybrid energy storage system.

Robustness With Uncertain BSM-HESS Parameters

This section is to study the robustness of FLC under the uncertainty of BSM-HESS parameters. Particularly, a series of plant–model mismatches of battery/SMES series resistances $R_{L1}$ and $R_{L2}$, as well as inductances $L_1$ and $L_2$ with ±20% variation around their rated value are applied. Then, a 25% load drop occurs and lasts for 100 ms, during
which the absolute peak value of active power $|P|$ is recorded, as shown in Figure 6. Note that the changes of PID control and FLC under the uncertainty of series resistance are 11.31 and 31.86%, respectively.

**CONCLUSION**

In this study, an FLC is designed to realize an efficient and smooth power tracking for BSM-HESS, and its contributions are summarized as follows:

1. FLC can fully compensate the nonlinearity of the system to achieve a globally consistent control performance; thus, the transient performance can be considerably improved;
2. FLC requires an accurate BSM-HESS system model; thus, it lacks robustness against parameter uncertainties compared to PID control;
3. The effectiveness and superiority of FLC are comprehensively verified and compared with PID control based on three case studies. Simulation results show that FLC outperforms PID control in terms of overshoot and tracking rate.

In the future, the effectiveness of FCL will be further validated by a hardware-in-the-loop (HIL) experiment based on the dSpace platform to meet the practical needs of engineering application.

**DATA AVAILABILITY STATEMENT**

The original contributions presented in the study are included in the article/Supplementary Material; further inquiries can be directed to the corresponding authors.

**AUTHOR CONTRIBUTIONS**

CT: conceptualization, writing—original draft preparation, and investigation. YH: writing, reviewing and editing, supervision, and conceptualization.

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NOMENCLATURE

Variables
\( v_1, v_2, v_o \) voltages corresponding to \( C_1, C_2, \) and \( C_o \)
\( i_1, i_2 \) currents flowing through \( L_1 \) and \( L_2 \)
\( E \) open-circuit voltage of battery
\( I_{sc} \) SMES current

Abbreviations
BSM-HESS battery/SMES hybrid energy storage system
SMES superconducting magnetic energy storage
RBS rule-based strategy
PID proportional–integral–derivative
FLC feedback linearization control

BSM-HESS parameters
\( C_1, C_2, C_o \) filter capacitances of battery side, SMES side, and load
\( L_{SC} \) inductance of superconducting magnetic coil
\( L_1, L_2 \) inductances of battery side and SMES side
\( R_e \) inner series resistances of battery
\( R_{L1}, R_{L2} \) series resistances of battery side and SMES side
\( R_{on1}, R_{on2}, R_{on3}, R_{on4} \) MOSFET on-resistances for \( S_1, S_2, S_3, \) and \( S_4 \)
\( R_o \) equivalent load
\( D_1, D_2 \) duty cycle for the on-state of \( S_1 \) and \( S_3 \)

FLC parameters
\( \lambda_1, \lambda_2 \) control gains