Gluon Density in the Rescaling Model

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Abstract—The behavior of the gluon density in nuclei is investigated in the framework of the rescaling model.

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1. INTRODUCTION

The study of deep inelastic scattering (DIS) of leptons on nuclei reveals the appearance of a significant nuclear effect, which excludes the naive idea of the nucleus as a system of quasi-free nucleons (see for an overview, for example, [1, 2]). This effect was first discovered by the European Muon Collaboration [3] in the domain of valence quark dominance, so it was named as the EMC effect.

Nowadays there are two main approaches to study the EMC effect. In the first one, which is currently more common, nuclear parton distribution functions (nPDFs) are extracted from global fits (see a recent review [4] and references therein) to nuclear data using empirical parameterization of their normalizations and the numerical solution of the Dokshitzer–Gribov–Lipatov–Altarelli–Parisi (DGLAP) [5] equations. The second strategy is based on some models of PDFs (see various models, e.g., in [6–8] and in a review [9]).

Here we will follow the scaling model [7] based on the assumption [8] that the effective size of confinement of gluons and quarks in a nucleus is larger than in a free nucleon. Within perturbative QCD, it was found [7, 8] that this confinement scaling predicts that nPDF and regular (nucleon) PDFs can be related by simple scaling of the $Q^2$ argument. Thus, we can say that the rescaling model demonstrates features inherent in both approaches: within its framework, there are certain relationships between conventional and nuclear PDFs that arise as a result of a shift in values of the kinematic variable $Q^2$ and, at the same time, both densities obey the DGLAP equations.

Initially, the rescaling model was created for the valence quark dominance region $0.2 \leq x \leq 0.8$. Recently in [10, 11], its applicability was extended to a range of small values of $x$, where certain shadowing and antishadowing effects were found for the sea quark and gluon densities.

The purpose of this short paper is to apply the rescaling model to the recently published PDF parameterizations [12] and show the nuclear modification of the gluon density in a wider range of $x$.

2. SEA QUARK AND GLUON DENSITIES

Using the $Q^2$-evolution of PDFs for large and small values of $x$ (see [13, 14] and [15, 16] respectively, as well as the review in [17]), the new type of PDF parameterizations was constructed in [12]\textsuperscript{1}.

The sea quark and gluon parts can be represented as combinations of $\pm$ terms:

\begin{equation}
\begin{aligned}
f_a(x, Q^2) &= \sum_{\pm} f_{a,\pm}(x, Q^2), \quad a = q, g, \\
f_{q,-}(x, Q^2) &= \left[ A_\pm e^{\nu_\pm x} (1-x)^{m_{a,-}} \right], \\
&+ \left[ B_\pm(s) x \overline{\Gamma(x)} (1 + v_-(s)) \right] (1-x)^{\nu_-(s)}, \\
f_{g,-}(x, Q^2) &= \left[ A_\pm e^{\nu_\pm x} (1-x)^{m_{a,-}+1} \right], \\
&+ \left[ B_\pm(s) x \overline{\Gamma(x)} (1 + v_-(s)) \right] (1-x)^{\nu_-(s)},
\end{aligned}
\end{equation}

where

\begin{equation}
\begin{aligned}
B_{\pm}(s) &= B_{\pm}(0) e^{p_{\pm} s}, \quad p_{\pm} = p_{\pm}(Y_{\pm} + \hat{c}_\pm), \\
B_{\pm}(s) &= B_{\pm}(0) e^{p_{\pm} s}, \quad p_{\pm} = p_{\pm}(Y_{\pm} + \hat{c}_\pm),
\end{aligned}
\end{equation}

\textsuperscript{1} In a sense [12] is a continuation of previous studies [18] carried out for valence quarks.
with $\gamma$ being Euler's constant, $f$ is a number of active quarks, $\beta_0 = 11 - (2/3)f$ is the leading order of QCD $\beta$-function and
\begin{equation}
\begin{aligned}
r_+ &= \frac{12}{\beta_0}, \\
r_- &= \frac{16}{3\beta_0}, \\
\hat{s}_+ &= -\frac{\beta_0}{12}, \\
\hat{s}_- &= -\frac{3}{4}.
\end{aligned}
\end{equation}
Here $I_\nu (x)$ are the modified Bessel functions with
\begin{equation}
\begin{aligned}
\sigma &= 2\sqrt{d_+ \ln \frac{1}{x}}, \\
\rho &= \frac{\sigma}{2\ln(1/x)}, \\
d_+ &= \frac{12}{\beta_0}, \\
\hat{d}_+ &= 1 + \frac{20f}{27\beta_0}, \\
d_- &= \frac{16f}{27\beta_0}.
\end{aligned}
\end{equation}
The factors $\sigma_0^2, A_\nu (0)$ and $v_\nu (0)$ are free parameters obtained in [12]. The $Q^2$ dependence of the subasymptotic terms $\sim D_\nu (s)$ is taken from the momentum conservation law. In [12] $m_{q-, g-} = m_{g, q+} = 2$ and $m_{q+, g+} = 1$. In this case, the small $x$ asymptotics are suppressed at large $x$ compared to the subasymptotic terms $\sim D_\nu (s)$. Moreover, the small $x$ asymptotics contain the same powers of the factor $(1 - x)$ for quarks and gluons.

3. RESCALING MODEL

In the rescaling model [7], the DIS structure function $F_2$ and, consequently, the valence part of quark densities are modified in the case of a nucleus $A$ at intermediate and large values of $x$ ($0.2 \leq x \leq 0.8$) as follows
\begin{equation}
f_{A}^A (x, Q^2) = f_{A}^A (x, Q^2_{A, V}),
\end{equation}
where the new scale $Q^2_{A, V}$ is related to $Q^2$ by [10]
\begin{equation}
S_{AV}^{A} = \ln \frac{Q^2_{A, V} / \Lambda^2}{Q^2 / \Lambda^2} = s + \ln(1 + \delta_{AV}^{A}) = s + \delta_{AV}^{A},
\end{equation}
i.e. the kernel modification of the main variable $s$

3.1. Rescaling Model at Low $x$

In [10] the PDF asymptotics for small $x$ shown in (1) were applied to the small $x$ region of the EMC effect using the simple fact that the rise of sea quark and gluons densities increases with increasing values

In this case, the small $x$ asymptotics are suppressed at large $x$ with the subasymptotic terms $\sim D_\nu (s)$. Since there are two components for each parton density (see Eq. (1)), we have two free parameters $Q^2_{A, S}$ that can be determined from the analysis of experimental data for the EMC effect at low $x$ values.

Note that it is usually convenient to study the following ratio
\begin{equation}
R_{A}^{A} (x, Q^2) = \frac{f_{A}^{A} (x, Q^2)}{f_{g}^{A} (x, Q^2)}.
\end{equation}

Taking advantage of the fact that the nuclear effect in a deuteron is very small (see discussions in [9])
\begin{equation}
f_{d}^{A} (x, Q^2) = f_{g}^{A} (x, Q^2),
\end{equation}
we can assume that
\begin{equation}
f_{A}^{A} (x, Q^2) = f_{A}^{A, +} (x, Q^2) + f_{A}^{A, -} (x, Q^2),
\end{equation}
where
\begin{equation}
f_{A}^{A, +} (x, Q^2) = f_{A}^{g} (x, Q^2_{A, +}),
\end{equation}

The expressions for $f_{A}^{g} (x, Q^2)$ are given in Eq. (1) and the corresponding values of $s_{AV}^{A}$ turned out to be

\begin{equation}
s_{AV}^{A} = \ln \frac{Q^2_{A, V} / \Lambda^2}{Q^2 / \Lambda^2} = s + \ln(1 + \delta_{AV}^{A}),
\end{equation}

4. RESULTS

The results obtained for $R_{A}^{A} (x, Q^2)$ are shown in Fig. 1. As one can see, our results are very close to the results obtained in [10] at $x \leq 10^{-2}$, since the parame-
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CONFLICT OF INTEREST

The authors declare that they have no conflicts of interest.

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In addition, we study nuclear modifications of unintegrated PDFs [12, 23], which are now becoming very popular (see [24] and references and discussions therein).

However, we see a discrepancy between our results and the results of [4] at large values of $x$: $x \geq 0.1$. This must be due to the use of the $\delta^4_{x \simeq 0.1}$ parameters, which were obtained in [10] only during the study of the experimental data [20, 21] obtained at small $x$ values. In addition, since the [20, 21] data were obtained at very low $Q^2$ values, the quality of the fit performed in [10] is not very good. For example, the fitting results obtained using two different infrared modifications of the strong coupling constant: analytical and “frozen”, (see [22] and discussions therein) are very different, which is very unusual. We hope to study this phenomenon in our future publications, where we plan to take into account the new parametrizations (1) that are valid over the entire $x$ range and experimental data [3, 20, 21] from different ranges of the Bjorken variable $x$.

In addition, we plan to study nuclear modifications of unintegrated PDFs [12, 23], which are now becoming very popular (see [24] and references and discussions therein).

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