DIRECT IMAGING OF A COLD JOVIAN EXOPLANET IN ORBIT AROUND THE SUN-LIKE STAR GJ 504

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ABSTRACT

Several exoplanets have recently been imaged at wide separations of >10 AU from their parent stars. These span a limited range of ages (<50 Myr) and atmospheric properties, with temperatures of 800–1800 K and very red colors (J − H > 0.5 mag), implying thick cloud covers. Furthermore, substantial model uncertainties exist at these young ages due to the unknown initial conditions at formation, which can lead to an order of magnitude of uncertainty in the modeled planet mass. Here, we report the direct-imaging discovery of a Jovian exoplanet around the Sun-like star GJ 504, detected as part of the SEEDS survey. The system is older than all other known directly imaged planets. Its projected separation of 43.5 AU exceeds the typical outer boundary of ~30 AU predicted for the core accretion mechanism. GJ 504b is also significantly cooler (510 ± 20 K) and has a bluer color (J − H = −0.23 mag) than previously imaged exoplanets, suggesting a largely cloud-free atmosphere accessible to spectroscopic characterization. Thus, it has the potential of providing novel insights into the origins of giant planets as well as their atmospheric properties.

Key words: planetary systems – stars: formation – stars: individual (GJ 504)

1. INTRODUCTION

More than 890 extrasolar planets (or exoplanets) have been discovered by now (Schneider et al. 2011), and NASA’s Kepler mission alone has recently added more than 2000 exoplanet candidates (Batalha et al. 2013). The vast majority of exoplanets have been discovered using indirect detection techniques that infer the presence of the exoplanet by monitoring the host star, such as planetary transits or radial-velocity variations. The techniques require observations over at least one orbital period, making them impractical for detecting long-period exoplanets at large separations. Meanwhile, in spite of the technical challenges, 8 m class telescopes equipped with adaptive-optics (AO) systems and/or coronagraphs have
Because massive exoplanets cool and fade with time, direct-imaging searches have been most successful around young stars. Mass estimates for young planets depend strongly on the assumed system age, planetary atmosphere models, and initial thermodynamic state, leading to large uncertainties in the inferred mass. Planetary-mass estimates conventionally assume a “hot start,” in which the planet is initially in a high-temperature, high-entropy (and hence, luminous) state (Baraffe et al. 2003; Burrows et al. 1997). However, recent theoretical models suggest that giant planets produced according to standard formation theories could initially be much colder (Marley et al. 2007; Fortney et al. 2008; Spiegel & Burrows 2012). The difference between the mass–luminosity relations of the “hot-start” and “cold-start” models decreases with exoplanet age; the models converge after \( \sim 100 \) Myr for a 5 \( M_{\text{Jup}} \) planet, and \( \sim 1 \) Gyr for a 10 \( M_{\text{Jup}} \) planet (Marley et al. 2007; Fortney et al. 2008; Spiegel & Burrows 2012).

Previously imaged exoplanets are all younger than 50 Myr (Marois et al. 2008; Lagrange et al. 2010; Carson et al. 2013). The hot-start models imply planetary masses (Marois et al. 2008, 2010; Lagrange et al. 2010), while cold-start models cannot reproduce the high observed luminosities (Marley et al. 2007; Spiegel & Burrows 2012). Therefore, their planetary status would be negated if the cold-start models apply at such young ages. Nevertheless, independent constraints, such as dynamical stability analysis in the case of the HR 8799 system (e.g., Fabrycky & Murray-Clay 2010; Marois et al. 2010; Sudol & Haghighipour 2012), in some cases can be used to exclude the coldest range of initial conditions and confine their masses to the planetary-mass regime. In addition, we note that neither hot-start nor cold-start models have been calibrated against dynamical mass estimates. These arguments suggest that no fully established model for estimating the masses of directly imaged planets exists as of yet. However, direct imaging of an older system with a well-determined age could remove much of the model uncertainty related to the unknown initial conditions.

A common feature of the previously imaged planets is large effective temperatures (\( > 800 \) K; Marois et al. 2008) and very red colors implying the presence of thick clouds in their atmospheres. Furthermore, they have generally been discovered as companions to massive (\( > 1.5 \) \( M_{\text{Sun}} \)) stars (e.g., Baines et al. 2012; Lagrange et al. 2010; Carson et al. 2013), and hence they populate a limited range in atmospheric conditions and host star properties. Widening this range would greatly enhance our understanding of the population of exoplanets in wide orbits.

Here, we report the detection of an exoplanet around the nearby Sun-like star GJ 504 using high-contrast near-infrared imaging on the Subaru Telescope. The projected separation of the planet (GJ 504b) is measured to be 43.5 AU from the star, and the mass of planet (GJ 504b) is estimated to be a few \( M_{\text{Jup}} \), because the system has an age of 160\(^{+350}_{-60}\) Myr, its mass estimate is only weakly dependent on the uncertainty of initial conditions in the cooling models of giant planets. In Section 2, we describe the properties of GJ 504. In Section 3, the observations and data reductions are detailed. Section 4 presents a derivation of the mass of GJ 504b and other interesting properties of this planet.

Section 5 investigates the atmospheric properties and possible origin of GJ 504b. Our results are summarized in Section 6.

2. GJ 504 STELLAR PROPERTIES

GJ 504 is an isolated G0-type main-sequence star. It has a mass of 1.2 \( M_{\text{Sun}} \) and an age of 160\(^{+350}_{-60}\) Myr. In the following sections, we will describe the stellar properties in more detail, including its age estimate. Table 1 summarizes the properties of GJ 504.

2.1. Age of GJ 504

For an isolated main-sequence star like GJ 504, several methods of age estimation can be imagined, including gyrochronology, chromospheric, or coronal activity, lithium abundance, kinematics, or isochrones. Among them, two particularly relevant age indicators for GJ 504 are gyrochronology based on stellar rotation, and chromospheric activity as traced by \( \text{Ca H and K} \) emission, and this study thus uses these indicators as the fiducial age estimators. Both stellar rotation and activity decline as a Sun-like star ages and sheds angular momentum in its stellar wind, and both age indicators have been accurately calibrated using stars in open clusters (Mamajek & Hillenbrand 2008, hereafter MH08). Chromospheric activity is powered by the stellar magnetic dynamo, which is closely related to the stellar rotation rate. Gyrochronology, which directly measures this rate, is therefore the most direct, and may be the most reliable, of our age estimators (MH08), and allows us to obtain a best estimate of 160\(^{+700}_{-60}\) Myr for the age of GJ 504. However, adopting the age as given by the star’s chromospheric activity in addition to that from gyrochronology, we conservatively adopt 160\(^{+350}_{-60}\) Myr as the age estimate of GJ 504 system (see Figure 1 for summary). We describe these age estimations in
detail below, along with several other age indicators that are less well suited for the purpose.

2.1.1. Gyrochronological Age

The rotation of a star slows as the star ages and the stellar wind carries away angular momentum. Gyrochronology, which estimates a star’s age from its rotation rate and $B-V$ color (i.e., mass), is generally considered to be the most direct, and possibly the most accurate, method for inferring stellar age (MH08). Chromospheric and X-ray activity are powered by the stellar dynamo, which is closely related to the star’s rotation rate. Indeed, chromospheric age estimators often use stellar activity to infer the rotation period, which is then used to infer an age (MH08). The rotation period of GJ 504 has been derived by utilizing several stellar clusters, while Meibom et al. (2009) used only a single cluster.

To rigorously establish the age of GJ 504, we use three gyrochronology relations independently proposed (MH08; Barnes 2007; Meibom et al. 2009). All the relations determine a stellar age as a function of rotation period and $B-V$ color. Using the rotation period (3.329 days) and $B-V$ color (0.585 ± 0.007) of GJ 504, we derive ages of 140–180 (MH08), 110–230 Myr (Meibom et al. 2009), and 110–230 Myr (Meibom et al. 2009), respectively. The error ranges for the age estimates were derived based on all the possible sources of error: the observed scatter in the period–age relation (0.05 dex; MH08) or errors of coefficients in the period–age function (Barnes 2007; Meibom et al. 2009), and the error of the $B-V$ color. Conservatively adopting all these ranges, we estimate the age of GJ 504 to be 160^{+70}_{-60} Myr.

For the optimal value of the gyrochronological age estimation, we adopt 160 Myr, which was calculated by MH08, because MH08 have updated the gyrochronological relation of Barnes (2007). Both relations of MH08 and Barnes (2007) have been derived by utilizing several stellar clusters, while Meibom et al. (2009) used only a single cluster.

\begin{table}
\centering
\caption{Properties of GJ 504 System}
\begin{tabular}{lll}
\hline
Property & Primary & Planet \\
\hline
Spectral type & G0V$^a$ & late T–early Y \\
Distance (pc) & 17.56 ± 0.08$^b$ & \\
Proper motion (mas yr$^{-1}$); $\mu_\alpha$, $\mu_\delta$ & $-338.83 ± 0.25$, 190.24 ± 0.21$^b$ & \\
Effective temperature; $T_\text{eff}$ (K) & 6234 ± 25$^c$ & 510^{+30}_{-20}$
\hline
Surface gravity; $\log g$ & 4.60 ± 0.02$^c$ & 3.9^{+0.4}_{-0.2}$
Luminosity; $\log (L/L_\odot)$ & 0.332 ± 0.032$^c$ & $-6.09^{+0.06}_{-0.08}$
Metallicity; [Fe/H] & 0.28 ± 0.03$^c$ & \\
Adopted age (Myr) & 160^{+350}_{-60}$ & \\
Age by gyrochronology (Myr) & 160^{+350}_{-60}$ & \\
Age by chromospheric activity (Myr) & 330 ± 180 & \\
Mass & 1.22 ± 0.08 $M_\odot$ & 4.0^{+5.5}_{-1.5} $M_{\text{Jup}}$ \\
J-band mass & ... & 3.5^{+3.5}_{-1.5} $M_{\text{Jup}}$
H-band mass & ... & 3.0^{+4.0}_{-1.0} $M_{\text{Jup}}$ \\
$K_s$-band mass & ... & 6.5^{+5.0}_{-3.0} $M_{\text{Jup}}$
$L'$-band mass & ... & 3.5^{+4.0}_{-1.0} $M_{\text{Jup}}$
NIR brightness$^c$ (mag) ($J$; $\sim$1.2 $\mu$m) & 4.106 & 19.91 ± 0.15 \\
(H; $\sim$1.6 $\mu$m) & 3.860 & 20.14 ± 0.14$^d$
($K_s$; $\sim$2.2 $\mu$m) & 3.808 & 19.19 ± 0.28 \\
($L'$; $\sim$3.8 $\mu$m) & 3.94 & 16.84 ± 0.19 \\
\hline
\end{tabular}
\end{table}

Notes.

$^a$ Valdes et al. (2004) and Takeda et al. (2005).
$^b$ van Leeuwen (2007).
$^c$ Valenti & Fischer (2005).
$^d$ GJ 504b’s effective temperature, surface gravity, bolometric luminosity, and mass are estimated by comparing its age (160^{+250}_{-50} Myr) and $J H K_s L'$-band magnitude with the most commonly used cooling model (Baraffe et al. 2003). For quantifying best estimates and lower/upper limits for all of these quantities, we apply the same calculation as described in Section 4.2.
$^e$ The provided errors of the stellar $J H K_s$ photometry are less than 0.01 mag (Kidger & Martín-Luis 2003), while $L'$ photometry was obtained in this work with an error of 0.09 mag (see Section 3.5).
$^f$ The $H$-band photometric magnitude is based on the weighted mean of the March and May values.
et al. 2009, 2011) are indeed in good agreement with GJ 504. Since gyrochronology is a largely empirical method, there could in principle be uncertainties involved in the methodology that are not accounted for in the calibrations. For instance, if we hypothesize that the calibration could be metallicity-dependent, this would lead to systematic errors for targets with significantly different metallicity from the calibration clusters. For the case of GJ 504, it has a non-extreme value in this regard, and hence it is unlikely to be subject to such uncertainties. Another possible systematic uncertainty in gyrochronology involves the fact that rotation is easier to detect in rapidly rotating systems, which could result in a bias in the empirical gyrochronology relation.

2.1.2. Chromospheric Activity Age

Stellar chromospheric activity, as traced by Ca II H and K emission, is a good indicator of stellar age. The strength of Ca II H and K emission is parameterized by \( R'_{\text{HK}} \), roughly the power in the H and K lines normalized to that in the underlying photospheric continuum. A relation between \( R'_{\text{HK}} \), \( B-V \) color, and age has recently been derived for solar-type stars (MH08). For GJ 504, we adopt the value of \( R'_{\text{HK}} = -4.45 \) measured at Mt. Wilson Observatory with a temporal baseline of 30 yr (Radick et al. 1998), the longest such baseline in the literature. In order to minimize the uncertainty in \( R'_{\text{HK}} \), the value for which the star has been monitored for the longest possible time should be adopted (see MH08), which also protects against accidentally adopting an outlier in the activity variation.

This activity level may be used to infer a Rossby number, the ratio of the stellar rotation period to the timescale of convective overturn, of 0.60 ± 0.10 following MH08. We use this result, together with a \( B-V \) color of 0.585 ± 0.007 (van Leeuwen 2007), to estimate an age of 330 ± 100 Myr. We further add a 0.2 dex scatter in this relation, estimated from clusters (MH08). We assume this scatter to be uncorrelated with other sources of error. As a result, we obtain a chromospheric age estimate of 330 ± 180 Myr.

Other studies using data from Mt. Wilson Observatory have measured \( R'_{\text{HK}} \) values of −4.443 (Baliunas et al. 1996) and −4.486 (Lockwood et al. 2007), which differ slightly from our adopted value of −4.45. The chromospheric activity level was also measured to be \( R'_{\text{HK}} = -4.44 \) using 14 yr of observations at Fairborn and Lowell Observatories (Hall et al. 2009). Many of these studies’ observational baselines overlap with the source of our adopted \( R'_{\text{HK}} \) value (Radick et al. 1998). Adopting the mean of these measurements would have little effect on our chromospheric age of 330 ± 180 Myr.

A primary uncertainty in age determination from chromospheric activity is long-term activity cycles, which may easily exceed the timescales over which the activity is measured, and thus may potentially provide a systematic error if the activity is measured at an extreme but is taken to represent the mean activity for the star. In addition, as in the case of gyrochronology, the stellar activity also depends on the metallicity, possibly contributing to the uncertainty. Since activity as an age estimator is thought to be closely related to gyrochronology through

\[ R'_{\text{HK}} = -4.45 \]

If this were a significant effect, it would cause the apparent mean rotation in a cluster of a given age to appear more rapid than it is in reality. Hence, age estimates for individual stars based on a relation calibrated against such clusters would result in an overestimation (i.e., an individual star would appear older than it really is). Given that no other age indicators imply a significantly younger age for GJ 504 this is also unlikely to be a real issue, but nonetheless, such uncertainties are important to keep in mind in the age analysis.

In addition to I-sequence stars, Figure 2 includes rotation data of C-sequence stars, which are widely scattered in the plot. However, the scatter is much smaller for the older clusters. GJ 504 is best represented by I-sequence stars, and young I-sequence stars such as provided in M35 or M34 (Meibom et al. 2009, 2011) are indeed in good agreement with GJ 504.
the stellar dynamo, the possibility of measuring both rotation (which is robust against activity cycles) and activity in the same star as for the case of GJ 504 can alleviate this uncertainty.

2.1.3. X-Ray Activity

Young solar-type stars are active X-ray emitters. As for Ca II H and K, a relation has been derived (MH08) between stellar age, color, and X-ray luminosity. The best estimate of the X-ray luminosity of GJ 504 comes from the ROSAT all-sky survey of nearby stars (Hünsch et al. 1999), which has provided a ratio of X-ray to bolometric power log \( L_X/L_{bol} = -4.42 \) (Messina et al. 2003). This X-ray activity may be used to infer a Rossby number of 0.54 \pm 0.25 (MH08) and lead to the age estimate of 90–530 Myr for GJ 504. Because the temporal baseline for the X-ray measurement is much shorter than for the multi-decade measurements of \( R'_{HK} \), the inferred Rossby number is much more uncertain. Therefore, we do not adopt this estimate based on the X-ray emission, although it is consistent with the estimate from other methods.

2.1.4. Lithium Absorption

The strength of lithium absorption lines declines as a star burns its primordial supply of lithium, providing another indicator of stellar youth (Soderblom 2010). However, many effects, such as variations in the primordial supply of lithium, the extreme sensitivity of early lithium burning to the stellar accretion history (Baraffe & Chabrier 2010), and the importance of non-local thermodynamic equilibrium abundance corrections (Takeda & Kawanomoto 2005), make it difficult to obtain a reliable age estimate from lithium abundances. Therefore, we do not employ lithium as an indicator to date GJ 504, but it can provide a clue to the age of GJ 504 as discussed below. The equivalent width of Li in GJ 504 has been measured to be 0.08 Å, implying a lithium abundance of \( \log(N(Li)/N(H)) + 12 = 2.9 \) (Takeda & Kawanomoto 2005). Extensive observations of well-dated open clusters (Sestito & Randich 2005) enable a lithium age estimate for GJ 504. At the effective temperature of a G0 star (~6000 K), these cluster estimates can be used to infer an age range of approximately 30–500 Myr, fully consistent with our gyrochronological and chromospheric age estimates.

2.1.5. Kinematics

GJ 504 is not currently identified as a member of any clusters or moving groups (MGs), making it impossible to use population-based age estimators. The kinematic velocity of GJ 504 \( (U = -38.6, V = 1.5, W = -18.0; Mishenina et al. 2004) \) is consistent with thin disk stars, thus providing no tight constraint on the age, but remaining consistent with the young age provided by gyrochronology and chromospheric activity.

2.1.6. Isochrones

Since stars evolve along mass tracks in an H-R diagram with age, a common age determination method is based on isochronal analysis. This method can provide reasonable estimates for old stars that have evolved significantly off the main sequence and very young stars that are still undergoing rapid contraction. However, it is generally not useful for stars near the zero-age main sequence (ZAMS), around which stellar evolution proceeds slowly (e.g., Soderblom 2010). Indeed, generic isochronal estimates in the literature are known to give erroneous ages for young stars by up to two orders of magnitudes.

As illustrative examples, we consider the cases of HD 152555, HIP 10679, and HD 206860. These are all early G-type (G0–G2) stars which are members of young MGs; hence they are similar types of stars to GJ 504 with well-determined young ages, and thus can be used for comparison to isochronal ages of e.g., Valenti & Fischer (2005). HD 152555 is a member of the AB Dor MG (e.g., Torres et al. 2008) with an age of 50–100 Myr, whereas Valenti & Fischer (2005) give an age of 4.0 Gyr. HIP 10679 is a member of the \( \beta \) Pic MG (e.g., Torres et al. 2008) with an age of \( \sim 10 \) Myr, whereas Valenti & Fischer (2005) give an age of 3.0 Gyr. Finally, HD 206860 is a member of the Her-Lya MG (e.g., López-Santiago et al. 2006) with an age of \( \sim 200 \) Myr, whereas Valenti & Fischer (2005) give an age of 3.1 Gyr.

In light of these large discrepancies, it is unsurprising that literature estimates for the isochronal age of GJ 504 vary strongly from hundreds of Myrs to several Gyrs (e.g., Valenti & Fischer 2005; Takeda et al. 2007; Holmberg et al. 2009; da Silva et al. 2012). This implies that isochronal analysis should simply be disregarded for a star such as GJ 504, compared to the more reliable age estimators listed above. Nonetheless, since some of the isochronal literature estimates provide Gyr-range ages that are seemingly inconsistent with the younger age range we have adopted for GJ 504, we discuss their application to this star in more detail below.

An important limiting factor in isochrone analysis for age determination of an isolated main-sequence star such as GJ 504 is the sensitivity to uncertainties in input stellar parameters. This is in particular true for properties such as effective temperature and surface gravity, where the uncertainties are model-dependent and often tend to be underestimated in the literature. As an illustration, we consider the isochronal analysis in da Silva et al. (2012) based on the Yonsei–Yale isochrones (Yi et al. 2001), which gives an age of \( \sim 3 \) Gyr, and appears to be inconsistent with ages of \( \leq 500 \) Myr within their quoted error bars. We have reproduced the analysis of da Silva et al. (2012) and confirmed these results with the same methodology and input observables. This is plotted in Figure 3. Also plotted in the same figure is the exact same analysis, but using the temperature estimates of GJ 504 from Valenti & Fischer (2005) instead; note that all other values are kept as in da Silva et al. (2012). This comparison immediately illuminates one of the considerable uncertainties related to isochronal analysis, which is uncertainties in the temperature scaling. The two temperature estimates in Valenti & Fischer (2005) and da Silva et al. (2012) are inconsistent within their quoted error bars, implying that neither error estimate should be trusted when translating this into an error on the age from the isochronal comparison. Moreover, we find that while the temperature estimate of da Silva et al. (2012) gives the aforementioned age of \( \sim 3 \) Gyr and is inconsistent with \( \leq 500 \) Myr ages, the temperature estimate of Valenti & Fischer (2005) is fully consistent with these younger ages, and inconsistent with the \( \sim 3 \) Gyr age.
Furthermore, while the temperature and luminosity in da Silva et al. (2012) gives a certain age from comparison with the Yonsei–Yale isochrones, this does not account for the relatively high surface gravity they quote. We can see this in the second panel of Figure 3, where again we perform an isochronal analysis, but in surface gravity versus temperature as opposed to luminosity versus temperature. Here, regardless of which temperature value is used, the data are consistent with a 500 Myr age, but inconsistent with a ~3 Gyr age.

It is instructive to think of these discrepancies in terms of the radius of the star. If we adopt the da Silva et al. (2012) temperature, then the luminosity is high for its mass, implying a large radius. On the other hand, the surface gravity is also high for its mass, implying a small radius. Hence, there is a tension in the radius between the luminosity and surface gravity if the da Silva et al. (2012) temperature is adopted, such that no self-consistent picture can be reached by either increasing or decreasing the stellar radius. By contrast, if we adopt the Valenti & Fischer (2005) temperature, then this tension disappears, and a self-consistent picture can be reached between the temperature, luminosity, and surface gravity—and simultaneously, we obtain a predicted age which is consistent with the estimates given by the age estimates in the previous sections. This could therefore be interpreted as supporting the higher temperature of Valenti & Fischer (2005) and thus a younger age.

Hence, we note that the isochronal age is readily consistent with gyrochronology and activity, using values for temperature, luminosity, and surface gravity published in the literature. This is also consistent with the arguably most detailed Bayesian isochronal analysis of Takeda et al. (2007), which was a study meant to improve on the analysis of Valenti & Fischer (2005) using the same input data, and which gives an age limit of <760 Myr. Nonetheless, the above discussions imply that it is not feasible to provide age constraints from isochronal dating that are as meaningful nor as stringent as those of gyrochronology and chromospheric activity. Thus, we do not include it in our adopted age range, but merely conclude that it is broadly consistent with such an age.

Finally, it can be noted that the existence of a star with such a short rotation period as GJ 504 (~3 days) would be unprecedented at the Gyr scale ages predicted by some isochrone analyses, such as da Silva et al. (2012). Indeed, although Reiners & Giampapa (2009) found an unusually rapid rotator in the ~4 Gyr old M67 cluster, it has a rotation of approximately half the solar rotation rate (P_solar ~ 30 days), which is significantly slower than the rotation of GJ 504. Aside from known close spectroscopic binaries, it is the largest known outlier at such an age. No indications of chromospheric activity corresponding to such rapid rotation have been found among 60 stars in the M67 cluster (Giampapa et al. 2006), which supports the notion that rapid rotators like GJ 504 must be exceedingly rare at ages of a few Gyr.

2.1.7. Summary of Age Estimate for GJ 504

As discussed above, we adopt the age estimated with gyrochronology as the most likely age (160±30 Myr) for GJ 504. However, we conservatively adopt an age of 160±50 Myr, with chromospheric activity providing the upper bound and gyrochronology providing the lower bound. Age indicators based on the lithium abundance, X-ray luminosity, kinematics, and isochrone technique are less precise than gyrochronology and chromospheric activity: in addition, for the Li-age estimate it is more difficult to quantify the uncertainty. We therefore do not attempt to combine those with the age range estimated from the gyrochronological and chromospheric activity techniques, although their estimates are consistent with our adopted age of GJ 504. Future asteroseismology studies, or detailed kinematic studies identifying GJ 504 as a member of an MG, may be able to refine our age estimate. The estimated ages are summarized in Table 1 and Figure 1.

2.2. Other Information

GJ 504 was previously reported to have a stellar companion at a projected separation of about 650 AU (Poveda et al. 1994), but subsequent observations showed that it does not share a common proper motion; the GJ 504 proper motions are −333.83 ± 0.25 mas yr⁻¹ and 190.24 ± 0.17 mas yr⁻¹ in right ascension and declination (van Leeuwen 2007), respectively, while those of the stellar companion candidates are 22.9 ± 11.2 mas yr⁻¹.
24 μA recent estimate based on the empirical function for GJ 504. Interestingly, GJ 504 has a super-solar metallicity [Fe/L] = 0.28 (Valenti & Fischer 2005). In order to estimate the mass of the central star, we use an empirical relation of Torres et al. (2010), which is a function of the surface gravity, effective temperature, and metallicity of GJ 504 (Valenti & Fischer 2005). The error of the estimate was provided by correlations of the best-fit coefficients (Fleming et al. 2010). Hence, we identify the stellar companion candidate as an unrelated background star.

The effective temperature, surface gravity, and metallicity [Fe/H] of GJ 504 were inferred by directly fitting the observed spectrum to the synthetic spectrum (Valenti & Fischer 2005). Interestingly, GJ 504 has a super-solar metallicity [Fe/H] = 0.28 (Valenti & Fischer 2005). In order to estimate the mass of the central star, we use an empirical relation of Torres et al. (2010), which is a function of the surface gravity, effective temperature, and metallicity of GJ 504 (Valenti & Fischer 2005). The error of the estimate was provided by including uncertainties in the spectroscopically determined input parameters, the reported intrinsic scatter in the relation, and correlations of the best-fit coefficients (Fleming et al. 2010). As a result, the mass of GJ 504 is estimated to be 1.22 ± 0.08 solar masses. The mass of GJ 504 can also be derived based on matching its spectroscopically determined surface parameters with theoretical stellar evolution models (Takeda et al. 2007; Valenti & Fischer 2005). The theoretical models infer the mass of GJ 504 to be 1.29 ± 0.05 M\(_{\odot}\) (Takeda et al. 2007) or 1.28 ± 0.03 M\(_{\odot}\) (Valenti & Fischer 2005), overlapping with the empirical estimate. For our analyses, we employ the mass estimate based on the empirical function for GJ 504.

Broadband observations of the infrared excess above the photosphere at 24 μm and 70 μm place constraints on the distribution of dust in the inner (<10 AU) and outer disks. A recent Spitzer survey showed that 4% of Sun-like stars have 24 μm excess, while 16% of Sun-like stars have 70 μm excess (Trilling et al. 2008). GJ 504 was shown to not have excesses at either of these bandpasses (L\(_{\text{dust}}\)/L\(_{\text{star}}\) < 2.1 × 10\(^{-6}\)), and therefore does not seem to harbor a significant debris disk (Bryden et al. 2006).

### 3. Observations and Data Reduction

GJ 504 was observed as part of the Strategic Exploration of Exoplanets and Disks with Subaru (SEEDS) survey (Tamura 2009), which aims to detect and characterize giant planets and circumstellar disks using the 8.2 m Subaru Telescope. In 2011 and 2012, we obtained J- (~1.2 μm), H- (~1.6 μm), and K\(_{s}\) (~2.1 μm) band images using the High Contrast Instrument for the Subaru Next Generation Adaptive Optics (HiCIAO; Suzuki et al. 2010) with AO188, a 188 actuator AO system (Hayano et al. 2008). Furthermore, we obtained follow-up L′-band (~3.8 μm) images using InfraRed Camera and Spectrograph (IRCS; Kobayashi et al. 2000) and AO188. See Table 2 for the summary of GJ 504 observations.

### 3.1. HiCIAO Observations

We discovered GJ 504b in H-band observations using HiCIAO on 2011 March 26 with AO188. We used GJ 504, its host, as the natural guide star, and used an atmospheric dispersion corrector (ADC) to prevent it from drifting on the detector due to differential refraction in the visible and near-infrared. We used a circular occulting mask 0′.4 in diameter and angular differential imaging (ADI; Marois et al. 2006) to remove the starlight and the stellar speckles. ADI keeps the telescope pupil fixed relative to the camera, while the field of view (FoV) rotates as the target moves across the sky. As a result, diffraction and speckle patterns in the stellar point-spread function (PSF), caused by the major part of telescope optics, remain fixed on the detector while real on-sky sources, such as a planet, rotate about the natural guide star. This allows ADI data processing to distinguish between stellar speckles and real objects, and to remove the starlight while preserving potential planets.

We conducted several follow-up observations in 2011 and 2012 using the same instrument and configuration. H-band follow-up observations were performed on 2011 May 22. The new H-band observations had both a longer total exposure time and better AO performance than the March observations, giving a higher signal-to-noise ratio (S/N) in the final images. We obtained the K\(_{s}\) and J-band data in 2012 February and April. The seeing in the J-band observation was among the best ever measured during SEEDS observations, and the AO worked very well, but those in K\(_{s}\)-band observations were worse than J- and H-band observations.

To correct the optical distortions of HiCIAO (and IRCS), we observed the globular cluster M5 using both instruments and compared the results to distortion-corrected images taken using the Advanced Camera for Surveys (ACS) on the Hubble Space Telescope; the accuracy and calibration for plate scale, orientation angle, and distortion of ACS/WFC camera, whose data were used for our calibration, had been previously reported (van der Marel et al. 2007). The distortion-corrected plate scale was 9.500 ± 0.005 mas pixel\(^{-1}\) for HiCIAO, and its north orientation was 0:35 ± 0:02. Uncertainties in the distortion correction are less than 4 mas for HiCIAO within the central 10″ × 10″ of the FoV. We have included all of these uncertainties in our positional measurements for the planet detected in both HiCIAO and IRCS images, though they have little effect on our results. Photometric calibrations were performed by observing the central star itself with neutral density (ND) filters with transmissions of 0.590, 0.0628, and 1.14% for J, H, and K\(_{s}\) bands, respectively.

| Obs. Date (UT) | Inst. | Band | Total DIT (min) | Mode | FRA (′) | Proj. Sep. (arcsec) | P.A. (′) |
|---------------|-------|------|----------------|------|---------|--------------------|---------|
| 2011 Mar 26   | HiCIAO| H    | 12             | ADI  | 52.7    | 2.479 ± 0.016      | 327.94 ± 0.39 |
| 2011 May 22   | HiCIAO| H    | 21             | ADI  | 56.9    | 2.483 ± 0.008      | 327.45 ± 0.19 |
| 2011 Aug 12   | IRCS  | L′   | 7              | DI   | ...     | 2.481 ± 0.033      | 326.84 ± 0.94 |
| 2011 Aug 15   | IRCS  | L′   | 19             | DI   | ...     | 2.448 ± 0.024      | 325.82 ± 0.66 |
| 2012 Feb 28   | HiCIAO| K\(_{s}\) | 38          | ADI  | 42.5    | 2.483 ± 0.015      | 326.46 ± 0.36 |
| 2012 Apr 12   | HiCIAO| J    | 40             | ADI  | 66.1    | 2.487 ± 0.008      | 326.54 ± 0.18 |
| 2012 May 25   | IRCS  | L′   | 68             | ADI  | 129.0   | 2.499 ± 0.026      | 326.14 ± 0.61 |

Notes. The dates, used instruments, observation bands, total detector integration times (DIT), observation modes, and field rotation angles (FRA) are summarized for each observation run. The measured projected separations and position angles (P.A.s) are also described.

and −51.7 ± 11.2 mas yr\(^{-1}\) in each direction (Roeser et al. 2010). Hence, we identify the stellar companion candidate as an unrelated background star.
3.2. IRCS Observations

To obtain data at a longer wavelength, we observed GJ 504 in the L′-band using IRCS on 2011 August 12 and 15. We did not use either ADI or an occulting mask during these long-wavelength observations. In addition, we obtained each frame by dithering the target within the FoV, which allowed us to better subtract the high thermal background (see below). In order to confirm whether we can obtain advantages for L′-band observational results by employing ADI, we performed additional L′-band observations in 2012 May 25. The longer total exposure time, compared to the 2011 observations, as well as the usage of ADI, led to a higher S/N.

As in the case of HiCIAO, we observed M5 to obtain the calibration data for correcting the distortion of IRCS. After the distortion-correction, IRCS has the plate scale of 20.54 ± 0.03 mas pixel−1, and its north orientation was tilted by 0.28 ± 0.09. Uncertainties in the distortion correction are less than 8 mas for IRCS within the central 10′′ × 10′′ of the FoV. Because the L′-band magnitude of GJ 504 has not been measured, we calibrated it using a standard star observed right before GJ 504 observations. As with HiCIAO observations, we then measured the flux of GJ 504 with an ND filter with a transmission of 0.67%.

3.3. High-contrast Data Reduction

3.3.1. HiCIAO Data Reduction

For the HiCIAO data reduction, we first removed stripe patterns (see Suzuki et al. 2010) emerged on each data frame, and subsequently performed the flat-fielding. After correcting the image distortion, we registered each data set to the centroid of GJ 504 A. For the HiCIAO observations, which used an opaque 0′4 diameter occulting mask, we estimated the relative frame centers by calculating cross-correlations of the frames as a function of positional offset. The AO188 and ADC kept the PSF extremely stable and well centered. For confirmation, we fit the linear and quadratic functions to the frame-to-frame positional offsets introduced by the mask field lens were confirmed with three binaries in the SEEDS samples. We did not attempt to remove the offsets, but we have instead considered both of the offsets in the measurements of positions by adding systematic errors of 3 mas to the image registration uncertainties. In total, for H-band observations, image registration conservatively contributed ~12 mas to our reported positional uncertainties for GJ 504b in March and ~6 mas in May. Those uncertainties are ~10 and ~6 mas in 2012 February (Ks) and April (J), respectively.

We used the Locally Optimized Combination of Images (LOCI) algorithm (Lafrenière et al. 2007) to reduce the HiCIAO data. LOCI constructs a model PSF for each frame using the other frames in that data set as references. The resulting PSF is locally a linear combination of the reference images, with the coefficients determined using a least-squares minimization. To avoid subtracting astrophysical sources, LOCI only uses reference frames with a minimum level of field rotation. For our reductions of GJ 504, we required at least 1.2 (=Nσ) × FWHM/R (×180/π deg) of field rotation, where the FWHM of PSFs on HiCIAO images is ~50–60 mas and R is the radial distance from GJ 504. As a result, any physical source was displaced by at least 1.2 FWHM between the working frame and the reference frames. We investigated if the S/N was improved by applying Nσ = 1.5 to the reductions but the S/Ns remained almost the same or were slightly reduced compared with the cases for Nσ = 1.2, and we thus carry out all analyses based on the images reduced with Nσ = 1.2.

For the H-band observations, our analysis of the data from March 26 detected a faint companion at an S/N of 5, where we calculated the noise as the standard deviation of the intensity in concentric annuli about GJ 504. Because of the longer integration time and better observing conditions for the observations in 2011 May, we detected GJ 504b with S/N = 9.0. We detected no other companion candidates (S/N ≤ 5) in either observation. GJ 504b is clearly confirmed with S/N of 18.4 at J-band, while the S/N of the Ks-band observations is 4.6.

The J, H, and Ks-band images for GJ 504b are shown in Figure 4. Also, the high-contrast two-color composite images is shown in Figure 5, in which GJ 504b is clearly visible 2′48 northwest of GJ 504.

3.3.2. IRCS Data Reduction

For the IRCS data, we first corrected flat-fielding. Subsequently, we subtracted the thermal background and then used an algorithm (Galicier et al. 2011) similar to LOCI in order to further reduce the background. We estimated the background value at each pixel and in each frame by dithering the images and using a linear combination of the frames in which the central source, GJ 504, is sufficiently displaced. As in LOCI, we computed the coefficients for this linear combination using a least-squares fit. Eventually, we subtracted the resulting estimate of the local background whose variation is a function of time. As in HiCIAO reductions, we subsequently corrected the distortion of IRCS images.

The IRCS L′-band data were taken without a mask, and were saturated out to a radius of about 3–4 pixels (∼60–80 mas, 0.6–0.8 FWHM, where FWHM is the full width at half-maximum of the PSF). We first performed relative registration by cross-correlating these saturated images with one another. We then centroided a set of unsaturated reference images, and cross-correlated the mean of these unsaturated PSFs with each saturated frame to measure the positional offset. Finally, the offsets introduced by the mask field lens were confirmed with three binaries in the SEEDS samples. We did not attempt to remove the offsets, but we have instead considered both of the offsets in the measurements of positions by adding systematic errors of 3 mas to the image registration uncertainties. In total, for H-band observations, image registration conservatively contributed ~12 mas to our reported positional uncertainties for GJ 504b in March and ~6 mas in May. Those uncertainties are ~10 and ~6 mas in 2012 February (Ks) and April (J), respectively.

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The J, H, and Ks-band images for GJ 504b are shown in Figure 4. Also, the high-contrast two-color composite images is shown in Figure 5, in which GJ 504b is clearly visible 2′48 northwest of GJ 504.
Figure 4. \(J\) - (~1.2 \(\mu\)m), \(H\) - (~1.6 \(\mu\)m), \(K_s\) - (~2.2 \(\mu\)m), and \(L'\)-band (~3.8 \(\mu\)m) images of the newly discovered exoplanet, GJ 504b. The four top panels show images reduced with the LOCI pipeline ((a) \(J\), (b) \(H\), (c) \(K_s\), and (d) \(L'\)). The corresponding signal-to-noise maps are shown on the four bottom panels ((e) \(J\), (f) \(H\), (g) \(K_s\), and (h) \(L'\)), in which the planet is detected with signal-to-noise ratios of 18.4, 9.0, 4.6, and 8.0, respectively. All signal-to-noise maps are shown at a stretch of (~5, 5). In all panels, the star is located approximately in the lower left corner. North is up and east is left.

Figure 5. Discovery images of the exoplanet GJ 504b. The central \(6'' \times 6''\) of two different high-contrast images were overlaid for this false color-composite image: orange represents \(H\) band (~1.6 \(\mu\)m; Subaru/HiCIAO; 2011 May 22), and blue represents \(J\) band (~1.2 \(\mu\)m; Subaru/HiCIAO; 2012 April 12). The \(J\)-band image was rotated by 0.9° to compensate for the planet’s observed orbital motion (cf. Figure 7). Panel (a) shows the intensity after suppressing flux from the central star. Panel (b) shows the associated signal-to-noise ratio (~9 in \(H\); ~18 in \(J\)). The orbital radius of Neptune (~30 AU) is shown for comparison with our own solar system. The planet GJ 504b is clearly visible as a white spot at a projected distance of 43.5 AU from the star GJ 504. The white color implies that the planet signal is persistent in both observations, setting it apart from the uncorrelated residual noise in each of the constituent images.
we applied this average offset to each of the saturated frames. The rms scatter of the offsets was ~6 mas for both observations in 2011 August, and ~4 mas for 2012 May. We adopt these scatterings as the registration uncertainties in \( L' \)-band data.

We then combined these registered frames. We detected GJ 504b with an S/N of 3 and 4.3 in the August 12 and August 15 data, respectively. Because the data for 2012 May 25 were obtained with ADI, we could use LOCI for the PSF subtraction before stacking the registered data: the LOCI reduction parameters were set to be the same as the case of HiCIAO. In the resulting image, the companion was clearly detected with an S/N of 8.0 (see Figure 4).

3.4. Positional Measurements of GJ 504b

We measured the position of GJ 504b by fitting two-dimensional elliptical Gaussian functions to the final reduced data. Uncertainties in these Gaussian centroids range from 2 to 44 mas, and dominate the total uncertainties in the position of GJ 504b. Sometimes, LOCI introduces artificial shifts of the companion positions (Soummer et al. 2011). Measuring positions of artificial companions, which have the similar brightness and locations with the GJ 504b, we have investigated how large offsets are added to the positions of GJ 504b. Because our adaptation for LOCI parameters is not aggressive and the planet’s separation is sufficiently large from the star \( r = 2''/48 \), the astrometric biases are not large. The positional measurements are converted to the projected separations and position angles (P.A.s) relative to the central star, and all of those are summarized in Table 2. Then, the uncertainties of measured separations and P.A.s were calculated by including the possible individual error sources of the image registration, distortion correction, plate scale, and orientation angle of each camera, and PSF-fit for GJ 504b.

3.5. Photometry

We performed aperture photometry on all of our observations of GJ 504b. For HiCIAO observations of the star GJ 504, we adopted magnitudes of 4.11, 3.86, and 3.81 for its \( J \)-, \( H \)-, and \( K_s \)-band brightness (Kidger & Martín-Luis 2003). The \( L' \)-band brightness of GJ 504 was calibrated with a standard star, so that we obtained \( L' = 3.94 \pm 0.09 \) mag for GJ 504. For all photometries of both the primary and the planet, we set the aperture radius to be 1.0 PSFFWHM, which ranged from 47 mas in \( J \) to 100 mas in \( L' \).

By subtracting (a local) linear combination of frames from each image, LOCI can artificially reduce the flux of a point source (Lafrénière et al. 2007). We limit this effect by choosing a relatively large \( N_s \) and estimate its magnitude using artificial point sources. We inject point sources in the HiCIAO data with projected separations and fluxes similar to those of GJ 504b, measuring their magnitudes before and after applying LOCI. We measured flux losses ranging from 13% to 23% for all LOCI reductions, where the typical scatter for the measurements of flux losses was 5%. We added this value to the final photometric errors. To verify this result, we re-reduced the HiCIAO data by subtracting a median PSF (Marois et al. 2006), but not applying LOCI. The resulting fluxes for GJ 504b had larger errors, but were consistent with their values in the final, LOCI-processed data. We estimated all of our photometric errors for the companion by calculating the rms scatter of aperture fluxes in blank-sky regions at the separation of GJ 504b. For the \( H \)-band data, these photometric errors were larger than the flux difference between the two sets of observations. For \( H \)-band observations, the unsaturated frames used to calibrate the companion fluxes were obtained before and after the main science sequences with the mask, while the unsaturated integrations for \( J \), \( K_s \), and \( L' \) bands were conducted in intervals among the main sequences as well. The total number of unsaturated frames that were used for photometric calibration was more than 31 for each epoch observation, except in 2011 March. We measured standard deviations of photometry of the primary using the unsaturated data; the worst value for the standard deviation was 22% in 2011 March, while these values were less than 12% in all other observations. We include these variations in the final photometric uncertainties, in addition to the errors of photometry for companion and self-subtraction estimates. For \( L' \)-photometry, we had three sets of images, but did not combine the result of 2012 with those derived from the data obtained in 2011, because the S/Ns of the \( L' \) images in 2011 were significantly worse than for the 2012 images; in the former case, no ADI was used and the observing conditions were very poor, with airmasses as high as 3.5 at maximum. Therefore, our adopted value for the \( L' \) photometry is based exclusively on the data obtained in 2012. The photometric measurements of GJ 504b at each band are summarized in Table 1, with the \( H \)-band flux computed using the weighted mean of the March and May values. Furthermore, the detection limits estimated from the reduced data are shown in Figure 6.

4. RESULTS

4.1. Astrometry

To confirm that GJ 504b is gravitationally bound to the host star, we tracked its proper motion over the course of more than a year, from 2011 March through 2012 May (Figure 7). Figure 7 allows to clearly visually distinguish the measured positions from the track expected for a background object. However, we also carried out a \( \chi^2 \) test to derive a statistical confidence that the source is a background star. This yielded a value of \( \chi^2 = 1340 \) (12 dof). Therefore, the \( \chi^2 \) test on the astrometry decisively excludes GJ 504b as an unrelated background source. On the other hand, if we assume GJ 504b to be an interloping foreground object, its color \( (\Delta H - \Delta L' = 3.3 \) mag) would rule out a star anyway, leaving only the possibility of a cool brown dwarf \( (T < 600 \text{ K}) \) within a distance of \( \sim 30 \text{ pc} \). Even under optimistic assumptions about the brown dwarf mass function (Kirkpatrick et al. 2011), less than one such object exists per \( 10 \) \( \text{ deg}^2 \), and the probability of a chance alignment within \( 3'' \) of GJ 504 is no more than \( 10^{-7} \).

Furthermore, in order to demonstrate that the measured motion of GJ 504b relative to its parent star GJ 504 is indeed consistent with the expected orbital motion of a gravitationally bound planet, we have fitted a Keplerian curve to its measured positions relative to the star, and constrained its orbit (see the Appendix). Here we assumed that the star has \( M = 1.22 M_{\odot} \). We show the best-fit curve in Figure 7. The best-fit \( \chi^2 \) was derived to be 11.7 (8 dof), which confirms that the measured positions relative to the central star are consistent with dynamical orbital
motion around the star. These analyses robustly prove that GJ 504 and GJ 504b comprise a physically associated system.

4.2. Mass Estimate

Using the luminosity and age of GJ 504b, we thus proceed to estimate its mass based on the hot-start model Baraffe et al. (2003, see Figure 8). We then calculate a mass by comparing the luminosity of GJ 504b at each band to the models, and eventually average the mass estimates at J, H, Ks, and L′ bands, which provides a mass of the planet, and its error range, which includes the errors from age and photometry. Any bias in the mass estimate caused by focusing on the photometry in a particular band should be mitigated when taking the average of the photometry of all bands. For the upper bound, we estimate the mass of GJ 504b from the 1σ bright end of the photometry at each band, using hot-start models for an age of 510 Myr. The collective upper limit is then acquired by averaging the estimates at each band. The lower limit is calculated in an equivalent way, using the 1σ faint end photometry and an age of 100 Myr. Likewise, the best estimate uses the mean photometry in each band and an age of 160 Myr. As a result of this procedure, a mass estimate of $4^{+5.5}_{-1.0} M_{\text{Jup}}$ is derived. The age uncertainty dominates the errors. If we adopt the gyrochronological age of 160$^{+70}_{-60}$ Myr, the most direct of our age indicators, the mass of GJ 504b is constrained to lie between 3 and 5.5 $M_{\text{Jup}}$. This is well below 13.6 $M_{\text{Jup}}$, the deuterium-burning threshold commonly used to divide planets and brown dwarfs (Marois et al. 2008; Burrows et al. 1997) and among the lowest masses for exoplanets discovered by direct imaging.

Adopting the Ks-band luminosity may result in a bias in the mass estimation, since this wavelength range is particularly sensitive to atmospheric parameters such as surface gravity and metallicity (Fortney et al. 2008; Spiegel & Burrows 2012; Janson et al. 2011). Indeed, Fortney et al. (2008) predict that raising the metallicity to five times solar metallicity results in a Ks-band brightening of a factor of two to six for a planet with temperature and surface gravity values in the range of what is expected for GJ 504b. Since the star GJ 504 has a metallicity above the solar value, it is very likely that the planet’s metallicity is also enhanced. For reference, if we neglect the Ks-band photometry, the best-fit mass of GJ 504b becomes 3.5 $M_{\text{Jup}}$, and is confined to be less than 8 $M_{\text{Jup}}$ based on the adopted age range.

The robustness of mass estimates for directly imaged exoplanets is usually limited by theoretical models used to derive age–luminosity relations. One uncertainty in these relations is the choice of initial conditions, which influences the estimation...
of a planetary mass. Since GJ 504 is older than 100 Myr, its inferred mass is less sensitive to the uncertainty in initial conditions for the employed model (Marley et al. 2007; Spiegel & Burrows 2012) than the previously imaged planets which have younger ages than GJ 504b. To test the sensitivity of the GJ 504b mass to uncertainties in the hot-start model, we compare the near-infrared luminosities of GJ 504b with a suite of models with ages between 100 and 510 Myr, initial thermal states...
Figure 9. Differences between mass estimates from cold-start models and hot-start models for 100 Myr old planets. The mass–luminosity relations modeled in Spiegel & Burrows (2012) are illustrated with dashed and solid lines for hot-start (entropy = 13 k_B baryon^{-1}) and cold-start (8 k_B baryon^{-1}) initial conditions, respectively. We show the relations for four atmosphere types on each panel ((a) J, (b) H, (c) K, and (d) L): “hybrid” means patchy cloud model and 1 or 3 S means one or three times solar-abundance model. The gray regions correspond to the absolute magnitudes of GJ 504b in each band and their error ranges (±1σ). The lower age limit (100 Myr) of GJ 504 is chosen in this illustration since that is the stage at which the largest differences occur between hot-start and cold-start conditions. As an example, the arrow in panel (b) indicates the difference in mass arising from different initial conditions when the 1S cloud-free model atmosphere is adopted. The difference is ∼4 M_{Jup}, which is also the median result for the full set of atmospheres and photometric bands.

mass estimates for 100 Myr old planets. The mass–luminosity relations modeled in Spiegel & Burrows (2012) are illustrated with dashed and solid lines for hot-start (entropy = 13 k_B baryon^{-1}) and cold-start (8 k_B baryon^{-1}) initial conditions, respectively. We show the relations for four atmosphere types on each panel ((a) J, (b) H, (c) K, and (d) L): “hybrid” means patchy cloud model and 1 or 3 S means one or three times solar-abundance model. The gray regions correspond to the absolute magnitudes of GJ 504b in each band and their error ranges (±1σ). The lower age limit (100 Myr) of GJ 504 is chosen in this illustration since that is the stage at which the largest differences occur between hot-start and cold-start conditions. As an example, the arrow in panel (b) indicates the difference in mass arising from different initial conditions when the 1S cloud-free model atmosphere is adopted. The difference is ∼4 M_{Jup}, which is also the median result for the full set of atmospheres and photometric bands.

5. DISCUSSION

Here, we discuss the unique properties of GJ 504b through comparison with other imaged planets. Furthermore, the possible origin of GJ 504 is discussed.

5.1. Previously Imaged Planet Candidates

Some of the previously imaged exoplanets were discovered around young (10–50 Myr), relatively massive stars like HR 8799 (1.5 M_{Sun}; 20–50 Myr; Marois et al. 2008, 2010) and β Pictoris (1.75 M_{Sun}; 10–20 Myr; Lagrange et al. 2010), with masses estimated at 5–9 M_{Jup}, assuming hot-start conditions. Recently, SEEDS detected a ∼13 M_{Jup} companion around the B9-type star Kappa And (2.5 M_{Sun}; 20–50 Myr; Carson et al. 2013). An exoplanet candidate around another massive star, Fomalhaut (2.0 M_{Sun}; ∼200 Myr; Kalas et al. 2008), has been detected at optical wavelengths. The images were reanalyzed by Galicher et al. (2013) and Currie et al. (2012), who recovered the point source at an additional wavelength. In addition, new optical images were recently presented with a report of an eccentric orbit (Kalas et al. 2013). Very recently, another imaged planet candidate has been reported around the young star HD 95086 (10–17 Myr; ∼1.6 M_{Sun}), but a robust second epoch confirmation still needs to be acquired (Rameau et al. 2013).
Figure 10. Comparison of multiple wavelength magnitudes of GJ 504b with cold-start model (Spiegel & Burrows 2012) predictions at the planet/brown dwarf boundary. In each panel, the cooling tracks predicted by the coldest-start models for a 14 $M_{\text{Jup}}$ planet are plotted in the age range of 20–500 Myr. Different panels correspond to the different bands ((a) $J$, (b) $H$, (c) $K_s$, and (d) $L'$). In addition, we show the cooling curves for four atmosphere types, where “hybrid” means patchy cloud model and 1 or 3 $S$ means one or three times solar-abundance model (Spiegel & Burrows 2012). The age range of GJ 504b is indicated by solid and dotted lines. The solid lines and dotted lines correspond to the age range inferred with gyrochronology (160$^{+70}_{-60}$ Myr) or chromospheric activity (330$^{\pm180}$ Myr), respectively. For comparison, we plot the brightness and age of HR 8799b (30$^{+20}_{-10}$ Myr) (Marois et al. 2008; Metchev et al. 2009) in each panel.

Other giant planet candidates have also been imaged at wide separations around very young (<10 Myr) stars (see, e.g., Kuzuhara et al. 2011). Among these, 1RXS J1609b (Lafrenière et al. 2008) orbits a pre-main-sequence solar-mass star at a wide separation of 330 AU.

For all the aforementioned companions, their masses have been inferred from comparisons of their infrared luminosity with hot-start models. However, due to the youth of those systems, they are highly affected by hot- versus cold-start conditions. The cold-start models imply that even HR 8799b, which may have the lowest masses among them, would be more massive than $\sim$14 $M_{\text{Jup}}$ (see Figure 10): its mass is estimated to be $\sim$20 $M_{\text{Jup}}$ or higher (except at $J$ band). Therefore, under cold-start assumptions, all the exoplanets around these young stars have much higher masses than currently inferred, and are pushed into the brown dwarf mass regime ($>\sim$14 $M_{\text{Jup}}$). One special case is the candidate around Fomalhaut, for which a mass below 3 $M_{\text{Jup}}$ has been reported, but deep infrared non-detections indicate that the detected light from the candidate cannot arise from a planetary surface (Janson et al. 2012); hence, its physical nature remains unclear. Regardless of the caution for the hot-start models, a few independent constraints, such as dynamical stability analysis in the case of the HR 8799 system (e.g., Fabrycky & Murray-Clay 2010; Marois et al. 2010; Sudol & Haghighipour 2012), suggest that the hot-start models may be realistic.

As discussed above, the mass estimates for directly imaged planets suffer from uncertainties of cooling models for giant planets until future calibrations may be obtained by comparing model-dependent masses with improved dynamical mass estimates. However, due to its old age, GJ 504b is less dependent on the models’ uncertainty related to the hot versus cold conditions, compared with previously imaged planets.

### 5.2. Color of GJ 504b

We can compare the magnitudes and colors of GJ 504b to similar objects in the literature in order to get a sense of the physical properties of this planet. For this purpose, it has been placed on color–magnitude diagrams (Figure 11) along with LT-type field brown dwarfs (Leggett et al. 2010) and HR 8799 bcde (Marois et al. 2010; Metchev et al. 2009; Skemer et al. 2012), Kappa And b (Carson et al. 2013), 1RXS J1609b (Lafrenière et al. 2008), 2M 1207b (Chauvin et al. 2004; Mohanty et al. 2007; Skemer et al. 2011), and GJ 758B (Thalmann et al. 2009; Janson et al. 2011).

Given the location of GJ 504b in the color–magnitude diagrams, it is clear that it is much colder than previous planet detections. Indeed, an application of $JHK_sL'$ luminosities of GJ 504b to those predicted by the cooling models of Baraffe et al. (2003) implies an effective temperature of $510^{+30}_{-20}$ K for the planet, where we estimated the best estimate and
and should be highly interesting for further atmospheric studies of GJ 504b thus places it in a physically distinct state from the cloudy regime. The cold and perhaps less cloudy atmosphere of GJ 504b (see Table 1), should lead to a clear atmosphere, while naturally in this temperature range (Allard et al. 2001). In the same temperature range (Leggett et al. 2010), which are color of GJ 504b is consistent with T-type brown dwarfs in temperature and surface gravity in Marley et al. (2012) do predict addition, models examining cloud clearing as a function of atmospheres (\(T_\text{eff} \sim 1000 \text{ K}\)) around HR 8799 or 2M 1207 may have thick clouds (Barman et al. 2011a; Madhusudhan et al. 2011; Skemer et al. 2011; Marley et al. 2012) although their cloud properties are under discussion (Barman et al. 2011a, 2011b). By contrast, the relatively blue \(J-H (= -0.23)\) color of GJ 504b is consistent with T-type brown dwarfs in the same temperature range (Leggett et al. 2010), which are representative of less cloudy atmospheres that could occur naturally in this temperature range (Allard et al. 2001). In addition, models examining cloud clearing as a function of temperature and surface gravity in Marley et al. (2012) do predict that a temperature of \(\sim 500 \text{ K}\) and log \(g\) of \(\sim 4\), as expected for GJ 504b (see Table 1), should lead to a clear atmosphere, while the properties of previously imaged planets place them in a cloudy regime. The cold and perhaps less cloudy atmosphere of GJ 504b thus places it in a physically distinct state from the hotter and cloudier atmospheres of previously imaged planets, and should be highly interesting for further atmospheric studies in the future. These properties imply that GJ 504b will become a benchmark object for the study of exoplanet atmospheres.

5.3. Implications for the Origin of GJ 504b

GJ 504b is a giant planet that lies at a projected separation of 43.5 AU. Two major scenarios could explain its formation: the core-accretion (CA) model (Pollack et al. 1996) and the gravitational instability (GI) model (Durisen et al. 2007). Here, we discuss whether the CA or GI can account for the origin of GJ 504b.

5.3.1. Core Accretion

In the CA model, the core of a giant planet accretes planetesimals and grows to a critical mass (\(\sim 10 \text{ Earth masses}\)), at which point the core begins to rapidly accrete gas directly from the protoplanetary disk. It is difficult for the CA model to explain the formation of giant planets in situ beyond 30 AU. A recent study (Dodson-Robinson et al. 2009) suggested that even a locally stable (but globally unstable) disk with an order of magnitude higher mass than the minimum mass solar nebula (Hayashi 1981) around a G-type star like GJ 504 was unable, in simulations, to form giant planets beyond 30 AU within the lifetime of the protoplanetary disk (Dodson-Robinson et al. 2009). Therefore, the presence of GJ 504b, as well as other directly imaged planets such as HR 8799 bcde, remains a particular challenge for the conventional CA theory. In this implication, we should note such numerical investigations as conducted by Dodson-Robinson et al. (2009) have typically neglected some theoretical processes that may enable the cores of giant planets to grow in the shorter timescale: effective damping of small planetesimal’s eccentricity due to gas drag (Rafikov 2004) or efficient capture of planetesimals due to atmospheric drag (Inaba & Ikoma 2003) may accelerate the accumulations of planetesimals in such the outer region, so that the in situ formation of GJ 504b may become possible (Rafikov 2011). However, even the models incorporating these processes may not necessarily be promising for producing a planet more massive than the critical mass beyond 30 AU at least for disks that are not particularly massive, as demonstrated by the simulations of Kobayashi et al. (2011).
Even if the in situ formation of a giant planet is difficult in such outer regions, models incorporating planet scattering can account for the origin of GJ 504b. If multiple planets are formed by CA in the inner regions, one or more of them could be scattered outward due to dynamical interactions among the planets (Nagasawa et al. 2008) or between the planets and the protoplanetary disk (Paardekooper et al. 2010; Crida et al. 2009). GJ 504b may have been pushed outward by as-yet undiscovered companions. Multiple giant planets may be common in metal-rich protoplanetary disks (Fischer & Valenti 2005), because the high metallicity may enhance solid materials and planetesimals in their protoplanetary disks, resulting in rapid growth of planetary cores. Eventually, outward migration may frequently occur in the metal-rich systems. Hence, the relatively high metallicity of GJ 504 system (see Table. 1) may be a preferential property to explain the origin of GJ 504b under the outward migration hypothesis.

5.3.2. Gravitational Instability

In contrast to CA, the GI model can form massive planets in situ at large radii. In this model, a massive protoplanetary disk becomes gravitationally unstable in its outer regions (∼50 AU) as the cooling time becomes short relative to the local dynamical timescale (Durisen et al. 2007). The outer disk then fragments, collapsing directly into one or more giant planets. The instability can also occur between 20 and 50 AU, with continuous inflows of gas into the magnetically inactive region inducing fragmentation on a timescale of ∼10^3 yr (Machida et al. 2011). However, the planet would have to escape the very rapid inward migration expected in a turbulent disk (Baruteau et al. 2011). In addition, if multiple massive planets are formed in the GI disk, they would still be scattered and eventually ejected from the systems, as in the case of CA. Therefore, GJ 504b would be a planet surviving against falling onto the central star or ejections form the system, if it was formed through the GI process. We should note that fragmentation could also be suppressed in a metal-rich disk like that expected for GJ 504; such a disk would cool less efficiently due to the higher opacities (Cai et al. 2006). Also, the significant gas accretion onto a clump formed according to the GI process may prevent the planet from remaining less massive (Zhu et al. 2012; Boley et al. 2010), disallowing the occurrence of a low-mass planet like GJ 504b.

5.3.3. Summary for Discussions of the Origin of GJ 504b and Future Prospect

Based on the available data, we cannot conclusively determine which process led to the formation of GJ 504b. However, it is interesting to note that GJ 504b is the first wide-orbit giant planet detected around a demonstrably metal-rich star. As discussed above, the high metallicity may enhance massive planetary cores, while preventing the effective cooling of a protoplanetary disk, and thus be more hospitable for CA formation than GI formation. Thus, given these measurable properties, planets such as GJ 504b may provide important clues for understanding the formation and evolution of giant planets.

For clarifying the origin of GJ 504b, the further observations may be crucial. Intriguingly, the CA model suggests the presence of unseen massive planets at smaller angular separations (Nagasawa et al. 2008; Chatterjee et al. 2008), making GJ 504 an outstanding candidate for follow-up observations by current and future instruments. N-body simulations for the dynamically unstable gas-free planetary system predict that such inner companions should orbit at a few AU from the host and have masses equal or greater than the corresponding outer planets (Nagasawa et al. 2008; Chatterjee et al. 2008). Therefore, the inner counterpart for GJ 504b would have to be more massive than ~4 M_Jup if it exists, although we note that radial-velocity observations have found few planets in this mass range at semi-major axes of a few AU (Mayor et al. 2011) and the remaining gasses in the disk may affect the scattering of planets, changing the configurations of planets predicted by the simulations for the gas-free cases (Moeckel & Armitage 2012).

Also, further monitoring of the orbit may be important, since scattered planets preferentially have high eccentricities (Chatterjee et al. 2008). Furthermore, modeling the atmosphere of GJ 504b may provide another piece of evidence to test whether it was produced by the CA process. The enhancement of heavy elements in the planetary atmosphere is a natural outcome of the CA process (Chabrier et al. 2007). It is possible to examine the abundances of such elements in the spectral energy distribution of GJ 504b through the use of atmospheric models. For this purpose, multiple wavelength photometric observations as well as the spectroscopy can play an important role.

Further observations of the GJ 504 system will constrain the origin of GJ 504b and may lead to a better understanding of the origin of planetary systems, including our solar system. Future instruments with direct (e.g., GPI, SPHERE, SCExAO) or indirect (e.g., IRD; Tamura et al. 2012) techniques that can explore more inner region may be able to find a promising evidence to clarify the origin of GJ 504b.

6. CONCLUSION

As part of the SEEDS direct-imaging survey, we have detected a giant planet around the Sun-like star GJ 504. The star has a spectral type of G0 and an approximate mass of 1.2 M_Sun. Its age has been conservatively estimated as 160+350 -60 Myr based on a combination of gyrochronology and chromospheric activity. Gyrochronology alone, which is the most direct and likely the most reliable age estimator, places the age at the lower end of this range, at 160+350 -60 Myr. Observations over one year baseline provided confirmation that the detected planet is orbiting the star. Compared with previously imaged exoplanets, GJ 504b has a number of interesting features.

1. The age of this planet is the oldest among all directly imaged planets.
2. Its mass is estimated to be 4+5.5 -1.0 M_Jup. This is among the least massive of imaged exoplanets. Because of its old age, the mass estimate is less dependent, compared to other imaged exoplanets, on the uncertainties of initial conditions in models used to convert its infrared luminosity into a mass.
3. GJ 504b is the first imaged giant planet on a wide orbit (>5 AU) around a G-type main-sequence star with a mass near the solar mass.
4. The planet’s projected separation from the primary is about 43.5 AU, which is comparable to the widest-orbit planets around massive stars such as HR 8799.
5. The effective temperature of the planet (510+30 -20 K) is the coldest among all previously detected giant planets.
6. The blue J − H color of −0.23 suggests that it has a less cloudy atmosphere than other imaged exoplanets. The cold temperature and color place the planet in a novel parameter space of atmospheres for exoplanets.

35 The current detection limit cannot explore giant planets in such the inner regions (see Figure 6).
7. GJ 504b is the first giant planet on a wide orbit discovered around a demonstrably metal-rich star.

The performed observations alone cannot conclusively uncover the origin of GJ 504b. Further observations of this system will enable more direct comparisons with our own solar system, and will help unveil the formation history of giant planets in the outer disk.

The authors thank Dr. I. N. Reid for discussions about age estimations of main-sequence stars. In addition, the authors have benefited from useful discussions with Drs. M. Ikoma, H. Nagahara, Y. Abe, S. Sugita, and B. Sato. Furthermore, the authors thank David Lafrenière for generously providing the source code for the LOCI algorithm. Our referee’s careful reading of the manuscript and excellent suggestions have improved the quality of this paper. The help from Subaru Telescope staff is greatly appreciated. This work was partly supported by KAKENHI 22000005 (M.T.), KAKENHI 23103002 (M.H.), WPI Initiative, MEXT, Japan (E.L.T), NSF AST 1008440 (C.A.G), and NSF AST 1009203 (J.C.), and NSF AST 1009314 (J.P.W.). Also, M.K. is partly supported by the Global COE program “From the Earth to Earths.” M.K., Y.H., Y.T., and J.K. are financially supported by the JSPS through the JSPS Research Fellowship for Young Scientists. Part of this work was carried out at the Jet Propulsion Laboratory, California Institute of Technology, under contract with NASA. Finally, the authors recognize and acknowledge the very significant cultural role and reverence that the summit of Mauna Kea has always had within the indigenous Hawaiian community. We are most fortunate to have the opportunity to conduct observations from this mountain.

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APPENDIX

MONTE CARLO ORBITAL ANALYSIS

To demonstrate that the measured motion of GJ 504b relative to its parent star GJ 504 is indeed consistent with the expected orbital motion of a gravitationally bound planet, we have run a Monte Carlo simulation following Janson et al. (2011). A large number of physically plausible orbits is randomly generated and compared to the astrometric data points. The maximum of the \( \chi^2 \) function is typically ill defined for an astrometric data set covering only a small fraction of an orbit: an entire family of orbits spanning a large range of semimajor axes match the data equally well. Thus, rather than ascribing an undue amount of significance to the simulated orbit with the smallest \( \chi^2 \) value, we consider the entire well-fitting family of orbits with \( \chi^2 < \chi^2_{\min} + 1 \). The plots in Figure 12 summarize the properties of this well-fitting orbit family.

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To characterize this distribution numerically, we determine the weighted median and the weighted 68% range for each parameter of the orbital simulation (semimajor axis \( a \), eccentricity \( e \), inclination \( i \), longitude of ascending node \( \Omega \), and argument of periastron \( \omega \)). We calculate the statistical weight \( W \) of each orbit as the mean orbital velocity divided by the local orbital velocity at the epoch of observation. This represents the fact that an eccentric planet orbits slower, spends more time, and is therefore more likely to be observed at apastron than at periastron.

However, some of the histograms are heavily skewed (e.g., log \( a \)) or even periodic (e.g., \( \Omega \)), as a result, the median badly represents the true behavior of the entire well-fitting orbit family. For this reason, we further define the most likely orbit (MLO). For each simulated orbit \( n \), we calculate as a measure of likelihood \( L_n \) the product of the histogram values of the log \( a \), \( e \), \( i \), \( \Omega \), \( \omega \) histograms in the bin into which the orbit falls, as well as the statistical weight \( W \):

\[
L_n = \text{hist}_{\log}(\log a_n) \cdot \text{hist}_e(e_n) \cdot \text{hist}_i(i_n) \\
\cdot \text{hist}_\Omega(\Omega_n) \cdot \text{hist}_\omega(\omega_n) \cdot W. \tag{A1}
\]

The MLO can then be defined as the orbit with the highest measure of likelihood, \( L_{\text{MLO}} = \max_n L_n \).
