Self-Doping Induced Orbital-Selective Mott Transition in Hg$_2$Ru$_2$O$_7$

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Pyrochlore oxides are fascinating systems where strong, multi-orbital correlations in concert with geometrical frustration give rise to unanticipated physical properties. The detailed mechanism of the insulator-metal transitions (IMT) underpinning these phenomena is, however, ill-understood in general. Motivated thereby, we study the IMT in the pyrochlore Hg$_2$Ru$_2$O$_7$ using LDA+DMFT. In contrast to the well-known examples of Mott transitions in TMO, we show that, in the negative charge-transfer situation characteristic of Hg$_2$Ru$_2$O$_7$, self-doping plays a crucial role in the emergence of an orbital-selective IMT. We argue that this mechanism has broader relevance to other correlated pyrochlore oxides.

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I. INTRODUCTION

The Mott-Hubbard insulator-metal transition (IMT) is by now recognized to play a central role in our understanding of d- and f-band compounds. Understanding the complex interplay between strong, multi-orbital (MO) electronic correlations, structural distortions, and strongly anisotropic, orbital-dependent hopping holds the key to a consistent theoretical description of their unique responses. Adding geometric frustration to the above results in a truly formidable problem. In geometrically frustrated systems, the exponentially large degeneracy of classical ordered states inhibits emergence of conventional order, permitting new, complex ordered ground states to arise. In real systems, structural effects may partially remove this huge degeneracy, making the problem (counter-intuitively) somewhat simpler to solve; however, in near-undistorted cases, near perfect orbital degeneracy, and the consequent strong quantum orbital and spin fluctuations in a highly degenerate system underpin their physical behavior.

The recently discovered pyrochlore system, Hg$_2$Ru$_2$O$_7$, is a particularly interesting case in this context. As temperature ($T$) is reduced, the anomalous (see below) non-Fermi liquid (nFL) metallic state becomes unstable, via a first-order Mott transition, to an antiferromagnetic Mott-Hubbard insulator (AFI). External pressure ($P_c = 6.0$ GPa, resulting in a low-$T$ correlated FL behavior for $T < T^* = 13$ K. At ambient pressure, the IMT transition is accompanied by lowering of lattice symmetry from (high-$T$) cubic to (low-$T$) a lower, hitherto precisely unknown, type: depending upon its precise type, either AF or dimer order may be possible.

The high-$T > T^*$ state in Hg$_2$Ru$_2$O$_7$ is an anomalous nFL: the dc resistivity, $\rho(T) \simeq T$ for $T > T_{MI} = 108$ K at ambient pressure, and deviates from the FL form for $T > T^*$ beyond $P_c$. The uniform spin susceptibility is Curie-Weiss like for $T > T_{MI}$, indicating a strong local moment scattering regime. The nFL character is also borne out from the recent photoemission (PES) data, showing anomalously broad PES lineshapes, with no hint of FL quasiparticles, in the metallic phase. Given the cubic pyrochlore structure for $T > T_{MI}$, strong orbital (from $t_{2g}$ orbital degeneracy) and spin fluctuations are implied. How might strong scattering processes involving these fluctuations produce the observed nFL metal? What drives the AFI as $T$ is lowered? A correlated electronic structure study which can illuminate these issues does not, to our best knowledge, exist. In this work we study precisely these issues in part in Hg$_2$Ru$_2$O$_7$ using the LDA+DMFT method. We focus on the mechanism of the T-driven IM transition, and leave the issue of the low-dimensional AF with a spin gap for future consideration.

II. MODEL AND SOLUTION

Starting with the high-$T$ cubic $Fd\bar{3}m$ structure found by Klein et al. local density approximation (LDA) band structure calculations were performed using a (scalar and fully-relativistic) full-potential local-orbital scheme (FPLO) and a linear muffin-tin orbitals (LMTO) scheme in the atomic sphere approximation. In Fig. 1 we display our FPLO-LDA results for the one-particle density-of-states (DOS). Clearly, the major contribution to the DOS comes from Ru(4$d$), O(1)(2$p$) orbitals, but the O(2)(2$p$) orbitals also have noticeable spectral weight at the Fermi level ($E_F$). As seen in Fig. 1 the influence of the spin-orbit coupling (SOC) in the cubic phase to the $t_{2g}$ states near $E_F$ is negligible. Further, we observe strong hybridization between Ru(4$d$) – O(1)(2$p$) orbitals, and between O(2)(2$p$) – Hg(6$s$) orbitals, but weak mixing between these two sets. These important findings will be exploited below to study the physics of Hg$_2$Ru$_2$O$_7$ using a multi-orbital Hubbard model involving only the d-band sector. At one-particle level, the corresponding model Hamiltonian reads, $H_{\text{band}} = \sum_{k,a,\sigma} \epsilon_{a} d_{k,a\sigma}^{\dagger} d_{k,a\sigma} + \sum_{i,a,b=1,2} \Delta_{b} (n_{i,b}^{p} - n_{i,a}^{d})$, where $a$ labels the diagonalized combination of $(\epsilon_{g1}, \epsilon_{g2}, a_{1g})$, the $t_{2g}$ orbitals, $\Delta_{b}$ ($b = 1, 2$) are the $pd$ charge trans-
fer (CT) terms involving two $Ru - O(1), (b = 1)$ and $Ru - O(2), (b = 2)$ channels. Clearly, neither an AFI Mott-Hubbard insulator nor a nFL metal can be expected at this level, this requiring a reliable treatment of strong, $d$-shell electronic correlations. This part reads,

$$H_{\text{int}} = U \sum_{i,a} n_{i,a}^d n_{i,a}^d + U' \sum_{i,a,a'} n_{i,a}^d n_{i,a'}^d - J_H \sum_{i,a,a'} S_{i,a} S_{i,a'}$$

with $a, a' = e_{g1}, e_{g2}, a_{g}$. Given the larger spatial extent of 4d-orbital vis-a-vis their 3d counterpart, we also include a Madelung term, $H_M = U_{pd} \sum_{<i,j>, a, b} n_{i,a}^d n_{j,b}^p$ in our calculations (see below). In $\text{Tl}_2\text{Mn}_2\text{O}_7$, the IMT (from a paramagnetic insulator (PI) to a ferromagnetic metal (FMM)) is seemingly driven by the $Tl(6s)$ states crossing $E_F$ across $T_c \frac{12}{17}$ for instance. This can occur via a $T$-dependent CT from the TM $d$-states to the $O(2)-Tl$ hybridized states. In view of the generic relevance of self-doping in TM 4$d$ pyrochlores, this term is an essential part. In the low-$T$ phase, this will involve CT processes involving the $O(2)p - Hg(6s)$ channel (second term of $H_{\text{band}}$) across the IMT, as we describe below.

The full many-body Hamiltonian reads $H = H_{\text{band}} + H_{\text{int}} + H_M$. We solve this model within MO dynamical mean field theory (MO-DMFT) developed and used for a range of TMOs with good success. We use the MO-iterated perturbation theory (IPT) as an impurity solver in the DMFT selfconsistent procedure. Though not numerically exact (like QMC, NRG, D-DMRG), it has many advantages: it is valid for $T = 0$, where QMC cannot be used. NRG/DDMRG are extremely prohibitive for three orbital models, even without electronic structural inputs at LDA level. As shown in earlier work, DMFT(MO-IPT) generically gives very good semi-quantitative agreement with PES/X-ray absorption (XAS) experiments for TMOs. For $\text{Hg}_2\text{Ru}_2\text{O}_7$, DMFT(MO-IPT) has to be extended to treat the second CT channel described above. Given the complexity of the problem, we choose the following strategy to solve $H$ above: For the high-$T$ phase, we (i) solve $H_{\text{band}} + H_{\text{int}}$ within DMFT(MO-IPT) version used earlier, for technical details see Ref. 15. (ii) As indicated by experiment on the related $\text{Tl}_2\text{Ru}_2\text{O}_7$ system, we study the effect of $\text{Ru}(4d) - \text{O}(2)(2p) - Hg(6s)$ CT processes by incorporating this CT channel selfconsistently into the LDA+DMFT(MO-IPT) procedure: given the small $\text{Ru}(4d) - \text{O}(2)(2p)$ hybridization, the $\text{O}(2)(2p) - Hg(6s)$ channel acts like a scattering (non-hybridizing) channel for the $\text{Ru} - t_{2g}$ bands in the impurity model of MO-DMFT. This enables us to treat this extra channel by combining the MO-IPT solution for (i) with the exact DMFT solution of a Falicov-Kimball model (FKM) for (ii) in a selfconsistent way.

### III. LDA+DMFT RESULTS AND DISCUSSION

![FIG. 1: (Color online) LDA band structure for cubic $\text{Hg}_2\text{Ru}_2\text{O}_7$. $O(1)$ ($O(2)$) denotes Oxygen ions nearest to $\text{Ru}$ ($\text{Hg}$).](image)

The $d_{\alpha\sigma}$ above should be understood as appropriate, $\text{RuO}_6$ cell-centered, combinations of the $4d$ and $O$-2$p$ orbitals, computed within LDA. Similarly, the $b = 2$ channel is to be understood as a band of hybridized $O$-2$p$ and Hg-6$s$ orbital states. Because of the negligible one-particle mixing (hybridization) between the $b = 1, 2$ channels, we approximate the full problem of three $Ru-d$ bands coupled to the $b = 2$ band channel by replacing the latter by a “reservoir”, whose only function is to simulate the self-doping process arising from the negative charge transfer situation that obtains in $\text{Hg}_2\text{Ru}_2\text{O}_7$. Of course, this is an approximation. It is, however, a good one: the $b = 2$ band channel has appreciably smaller DOS around $E_F$ in the LDA results. In a DMFT-like approximation, with negligible one-particle hybridization between the $b = 1, 2$ bands, the intersite Madelung term will push this small spectral weight away from $E_F$, to lower- and higher energy (notice that the $O-2p$ bands will be split by $U_{pd}z(n_d)$, where $z$ is the co-ordination number of the lattice, and hence quite large). This will already occur at the level of LDA+Hartree approximation. We then expect that the correlated spectral function will be dominated by the $d$-bands over an appreciable range about $E_F$. Correlation effects in $\text{Hg}_2\text{Ru}_2\text{O}_7$ via LDA+DMFT are studied below, subject to this caveat; we will show that this is indeed a good approximation a posteriori, in the sense that our LDA+DMFT results with the above caveat show very good quantitative agreement with one-particle spectroscopy and key thermodynamic and transport data in $\text{Hg}_2\text{Ru}_2\text{O}_7$.
the linear-in-$\rho T$ resistivities in this limit. The linear-in-quadratic behavior. This describes a nFL metal, with a Fermi energy ($\Sigma(\omega)$ shows frequency dependence near the Fermi energy ($|\omega - E_F| < 0.3$ eV), while $\text{Im}\Sigma_{\alpha\gamma}(\omega)$ shows quadratic behavior. This describes a nFL metal, with a linear-in-$T$ quasiparticle damping rate. Within DMFT, this is also the transport relaxation rate, since vertex corrections drop out in the computation of the conductivities in this limit. The dc resistivity is then given by $\rho_{dc}(T) \simeq (n^*/ne^2)\text{Im}\Sigma_{\epsilon'}(\omega = T) \simeq AT$, in accord with the linear-in-$T$ resistivity observed experimentally in the "high-$T$" metallic phase. Moreover, the selective localization seen in the $a_{1g}$ orbital DOS gives rise to unquenched local moments co-existing with “itinerant” (but incoherent as derived above) $\epsilon'_g$ carriers naturally gives a Curie-Weiss form of the spin susceptibility, which is also observed right up to the IMT. We have also estimated the $\gamma$-co-efficient of the metallic specific heat from the real part of $\Sigma_{\alpha}(\omega)$ (not shown) as $\gamma/\gamma_{\text{LDA}} = 4.25$: this seems to be in the range estimated in Ref 4. Actually, the noticeable $T$ dependence of $\gamma$ above $T_{MI} = 2.6$ is additional evidence of disordered local moments in the "bad" metal, and further supports our picture.

A. Metallic Phase

In Fig. 2, we show the correlated many-particle spectral function for the metallic phase of Hg$_2$Ru$_2$O$_7$. The dynamical spectral weight transfer (SWT) over large energy scales, characteristic of strong, local correlations is explicitly manifest. More interestingly, the metal has an orbital selective (OS) character: the $a_{1g}$ DOS is almost “Mott” localized, even as the $e_g'$ DOS develops a precursor of a low-energy pseudogap, characteristic of an incoherent metal behavior. This is further corroborated by examining the orbital dependent self-energies ($\Sigma(\omega)$), see inset in Fig. 2. Clearly, the $e_g'$ (imaginary part of) $\Sigma(\omega)$ shows quasi-linear frequency dependence near the Fermi energy ($|\omega - E_F| < 0.3$ eV), while $\text{Im}\Sigma_{\epsilon'_{\alpha}}(\omega)$ shows quadratic behavior. This describes a nFL metal, with a linear-in-$T$ quasiparticle damping rate. Within DMFT, this is also the transport relaxation rate, since vertex corrections drop out in the computation of the conductivities in this limit. The dc resistivity is then given by $\rho_{dc}(T) \simeq (n^*/ne^2)\text{Im}\Sigma_{\epsilon'_g}(\omega = T) \simeq AT$, in accord with the linear-in-$T$ resistivity observed experimentally in the "high-$T$" metallic phase. Moreover, the selective localization seen in the $a_{1g}$ orbital DOS gives rise to unquenched local moments co-existing with “itinerant” (but incoherent as derived above) $\epsilon'_g$ carriers naturally gives a Curie-Weiss form of the spin susceptibility, which is also observed right up to the IMT. We have also estimated the $\gamma$-co-efficient of the metallic specific heat from the real part of $\Sigma_{\alpha}(\omega)$ (not shown) as $\gamma/\gamma_{\text{LDA}} = 4.25$: this seems to be in the range estimated in Ref 4. Actually, the noticeable $T$ dependence of $\gamma$ above $T_{MI} = 2.6$ is additional evidence of disordered local moments in the "bad" metal, and further supports our picture.

Using the LDA+DMFT result, we also compare (Fig. 3) our computed PES lineshape, with very recent work from the RIKEN-SPring 8 group. Given our restriction to the $t_{2g} - Ru(4d)$ bands in the MO-DMFT ($Hg(d), O(2p)$ bands will start contributing at higher binding energies, as seen from LDA), good quantitative agreement with experiment is evident up to $-2.0$ eV, lending strong support to our theoretical work. Additionally, we predict that an intense peak will be seen around $0.4 - 0.5$ eV in X-ray absorption (XAS) studies, as in Tl$_2$Ru$_2$O$_7$.

In fact, the LDA+DMFT spectral functions show that, at low energy the full MO problem is mapped onto an effective FKM-like model, since the bad-metal is of the orbital-selective type. There, the problem in the local limit corresponds to itinerant (but incoherent) $\epsilon'_g$ carriers scattering off (Mott) localized $a_{1g}$ electronic states. The resulting problem is precisely the "X-ray edge" prob-
lem in DMFT.\textsuperscript{22} We now understand the structure of the self-energies, and the nFL behavior, as an interesting manifestation of the Anderson OC caused by this X-ray-edge mapping. Building upon this understanding, using DMFT, we predict that, for $T > T_{MI}$: (a) the optical conductivity will show a low-energy pseudogapped form, characteristic of an incoherent (nFL) metal. Polarised optical studies should indicate the OS-character of the nFL state, and, (b) given the local version of the Shastry-Shraiman relation\textsuperscript{24} the electronic Raman lineshape should show a continuum response, cut off by a pseudogap feature at low energy.

B. Insulating Phase

Now, we turn to a description of the insulating phase. A naive search for the instability of the nFL to a Mott-Hubbard insulating state, where $U, U'$ were increased to unphysical values, nevertheless turned out to be unsuccessful. This is a clear indication of involvement of additional, electronic-cum-structural effects in driving the IMT. The observed structural change across $T_{MI}$ supports this reasoning. From the LDA orbital assignment, it is clear that an additional structural change necessarily involves partial occupation of the two-fold degenerate $e'_g$ orbitals. Starting from the nFL-metal derived above, this can only occur via a $T$-dependent change in the “self-doping” process.\textsuperscript{25} As in $ThRu_2O_7$, this $T$-dependence could be provided by electronic coupling to the $Ru-O$ stretching phonon mode, which is experimentally observed to split below $T_{MI}$.\textsuperscript{14} This would imply a structural change setting in below $T_{MI}$, whose precise nature is hitherto unknown.

Motivated by this observation, we argue that this resulting change in the $Ru(4d) \rightarrow O(2)(2p)$ CT leads to a partial $4d$ occupation, induces orbital order, and lifts the $e'_g$ degeneracy via a structural distortion. Within DMFT, this will reduce the orbital-dependent hoppings, driving large SWT from low- to high energy, and stabilize the second, Mott-Hubbard insulating, solution of the DMFT equations. This is indeed seen in the LDA+DMFT calculation, as we show below.

Based on this reasoning, we explore the Mott-Hubbard insulating phase of $Hg_2Ru_2O_7$ by searching numerically for the instability of the first (metallic) solution found above to the second, insulating solution of the DMFT equations in the quantum paramagnetic phase. The DMFT(MO-IPT) equations are solved with $U, U', U_{pd}$, and $n_t = 2.6$. We vary $n_t$ in trial steps, and look for a critical $n_t^{(c)}$ which stabilizes the PI solution of the DMFT equations. As discussed above, and indeed seen in the inset of Fig.\textsuperscript{23} partial occupation of the $4d-e'_g$ orbitals leads to removal of the orbital degeneracy, and the corresponding modification of orbital orientation gives rise to a reduced intersite one-electron overlap. Within MO-DMFT, this triggers the Mott-Hubbard insulating state via large SWT on a scale of 5.0 eV, as seen in Fig.\textsuperscript{2}. Hence, the IMT is an OS Mott transition. Importantly, however, notice that the self-doping process leading to fractional $d$-orbital occupation is a crucial ingredient. Thus, in contrast to other OS cases,\textsuperscript{15} the IMT in $Hg_2Ru_2O_7$ is driven by the self-doping in the negative CT situation, $\Delta_2 = (\epsilon_{g2} - \epsilon_d) = (-2.8eV + 1.3eV) = -1.5eV$. Along with the microscopic elucidation of the nFL behavior, the agreement with PES in the nFL metal phase up to $\omega \approx -2.0 \, eV$ (Fig.\textsuperscript{2}) constitutes strong evidence in favor of our mechanism for the IMT in $Hg_2Ru_2O_7$. Quantitative comparison with PES in the low-$T$ phase requires an extension of our approach to include short-range (intersite) orbital and spin correlations characteristic of pyrochlores. This requires a cluster-DMFT analysis, presently a forbidding prospect. Nevertheless, observation of a Curie-Weiss spin susceptibility right up to the IMT also along with the excellent agreement with PES in the nFL, justifies the use of DMFT to describe the IMT.

We emphasize that this is a new picture for the IMT in correlated systems. In contrast to the early TMO, which are Mott-Hubbard insulators ($U_{dd} > \Delta$ in the Zaanen-Sawatzky-Allen scheme\textsuperscript{26} the $Ru(4d) - O(1)(2p)$ CT channel, along with the Madelung term, are important in $Hg_2Ru_2O_7$. In the DMFT context, the importance of the CT energy in the late-TMO is recognized.\textsuperscript{27} Our work is the first of its kind showing its relevance for the IMT in a MO pyrochlore system. Further, it is likely to be more broadly generic to pyrochlore TMOs; recall that, in $Tl_2Mn_2O_7$, the PI-FMM transition is driven by the shift of the $Tl(6s)$ band through $E_F$ across $T_c$. This is readily rationalized in our picture, in terms of the “switching on” the $Mn(3d) - O(2)(2p) - Tl(6s)$ CT channel across $T_c$ in $Tl_2Mn_2O_7$.\textsuperscript{28}

The correlation between the CT process detailed above and the IMT is also visible in a whole family of $4d$ pyrochlores, $A_2Ru_2O_7$, with $A = Pb, Bi, Y$.\textsuperscript{29} The low-$T$ magnetic ordering in the Mott-Hubbard insulating phase(s) may, however, be quite different, being sensitively dependent on the nature of the structural change across the IMT, as well as on spin state. For example, the spin $S = 1$ system, $Tl_2Ru_2O_7$, shows a very similar Mott transition; however, the low-$T$ phase is found to be a Haldane spin chain.\textsuperscript{30} In $Hg_2Ru_2O_7$, the half-integer spin $S = 3/2$ rules out the Haldane analogy. If the low-$T$ magnetic structure corresponds to having Ru chains, as in $Tl_2Ru_2O_7$, one would have an AF ground state with gapless spin excitations. Observation of the spin-gap in the uniform spin susceptibility in $Hg_2Ru_2O_7$ may therefore point to the relevance of the spin-orbit coupling in the insulating phase: this will induce Ising-like anisotropy in an $S = 3/2$ Heisenberg chain and generate a gap to spin excitations.\textsuperscript{31} More experimental work is also called for to pinpoint the specific factors affecting this issue. Given the structural distortion necessarily accompanying the IMT caused by lifting of the $e'_g$ degeneracy in $Hg_2Ru_2O_7$, more detailed theoretical work awaits more precise characterization of the low-$T$ structure of
Hg$_2$Ru$_2$O$_7$. We plan to address the issue of magnetic order and its associated excitation spectrum in the low-$T$ (insulating) phase of Hg$_2$Ru$_2$O$_7$ in a future work.

IV. CONCLUSION

In conclusion, we have performed LDA+DMFT calculations to demonstrate the role of multi-orbital electron-electron interactions on the electronic structure of a recently discovered pyrochlore system, Hg$_2$Ru$_2$O$_7$. This system exhibits a first-order temperature dependent MIT. The high-$T$ metallic phase is shown to be an orbital selective non-Fermi liquid, signalled by a quasi-linear frequency dependence of the imaginary part of the correlated self-energy and the absence of quasi-particle peaks in the orbital-selective spectral functions at very low frequencies. The LDA+DMFT spectral function shows good quantitative agreement with recent photoemission (PES) data, showing anomalously broad PES lineshapes, as well as with the linear-in-$T$ resistivity and mass enhancement in the metallic phase. In stark contrast to the better known examples of Mott transitions in 3d-transition metal compounds, our results imply a new mechanism for MIT in the 4d pyrochlore-based electron systems (like Hg$_2$Ru$_2$O$_7$). Namely, a negative charge-transfer associated self-doping drives an orbital-selective MIT at low temperatures via the Mott–Hubbard route. Our study should be more generally applicable to MO pyrochlore systems, and, in particular, to Tl$_2$Mn$_2$O$_7$, exhibiting Mott-Hubbard transitions as functions of suitable “tuning parameters”.

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