Termination-dependent surface in-gap states in a potential mixed-valent topological insulator: SmB$_6$

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We have investigated the surface states of a potential mixed-valent topological insulator SmB$_6$ based on first-principles density functional theory slab band structure analysis. We have found that metallic surface states are formed in the bulk band gap region, providing evidence for the topological insulating nature of SmB$_6$. The obtained surface in-gap states are quite different from those in existing reports in that they are formed differently depending on the Sm or B$_6$ surface termination, and are composed of mainly the Sm 4$f$ state indicating the essentiality of including $f$ electrons in describing the surface states. We have obtained the spin chiral structures of the Fermi surfaces, which are also in accordance with the topological insulating nature of SmB$_6$.

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I. INTRODUCTION

The low-temperature residual conductivity in a typical Kondo insulator SmB$_6$ has been a long-standing unresolved problem. In this respect, recent reports on the topologically protected metallic surface states in SmB$_6$ have attracted much attention [1–11]. Angle-resolved photoemission spectroscopy (ARPES) can provide direct evidence for topological insulators via observation of the Fermi surfaces arising from the surface in-gap states. Indeed, Fermi surfaces were observed in several ARPES studies at $\Gamma$ and $X$ points of the surface Brillouin zone (BZ) [2,3,12,13], supporting the topological Kondo insulating nature of SmB$_6$. Unfortunately, however, no explicit Dirac cone feature has been observed. Hence, some groups interpreted the metallic states observed in ARPES not as topological surface states but as bulk-shifted or normal (trivial) surface states [13,14]. Especially, the origin of the metallic bands at $\Gamma$ and $X$ is controversial as to whether they come from bulk or surface states [2,3,5,12,13]. Above all, the spin polarizations of the metallic surface bands have not been unveiled yet [4,15].

Among many difficulties, the surface instability in SmB$_6$ prevents revealing the topological nature. Since the chemical bonding between Sm and B$_6$ ions is not weak, the natural cleavage plane in SmB$_6$ is not well defined. The pristine Sm- and B$_6$-terminated surfaces, which are electrically polar and highly reactive, are likely to undergo disordered reconstructions or contaminations [16–18]. Due to this reason, the topological nature arising from the intrinsic surface states is not easily confirmed experimentally. Another difficulty with SmB$_6$ is the strong correlation effect of $f$ electrons. The highly renormalized $f$ bands require extremely high resolution ARPES experiments. Nevertheless, the topological invariance of SmB$_6$, which has been confirmed by a couple of theoretical studies [9,11], arouses great curiosity about the characteristics of the metallic surface states in SmB$_6$ [19].

There have been a few surface band calculations which tried to identify the topological properties of SmB$_6$. Takimoto [9] and Lu et al. [11] performed the (001) surface model calculations based on the density functional theory (DFT) and the DFT+Gutzwiller bulk band structures, respectively. Both of them obtained the metallic surface states in the bulk gap region, which produce three Dirac cones and the corresponding Fermi surfaces at $\Gamma$ and $X$. This feature suggests the nontrivial topological nature of SmB$_6$. But they considered neither the surface termination dependence nor the surface relaxation effect. Zhu et al. [14] performed the DFT slab calculations, and also obtained the surface states in the vicinity of the Fermi level ($E_F$). But their surface states come from the polarity-driven boron dangling bond, and so they claimed that the metallic surface states in SmB$_6$ are not the topologically protected surface states but the normal surface states. In their surface slab calculations, however, they considered the Sm $f$ electrons as core. Since the $f-d$ hybridization is essential to develop the insulating state in bulk SmB$_6$, it is likely that their surface band structures are not relevant to the $f$-electron system of SmB$_6$.

In this article, we have investigated systematically the (001) surface states of a potential mixed-valent topological insulator SmB$_6$, using first-principles DFT calculations on the slabs with different surface terminations. We have first compared the bulk band structures obtained by the DFT with those obtained by the dynamical mean-field theory (DMFT), whereby we have shown that the DFT is useful to investigate the low-energy band structure of strongly correlated mixed-valent insulator SmB$_6$. Then, we have performed the DFT surface band structure calculations, and found that the surface bands and the corresponding Fermi surfaces are quite different from those in the literature [9,11,14]. The gapless surface states are formed differently for the Sm-terminated case. We thus argue the importance of considering the Sm $f$ electrons and the termination dependence in describing the surface states of SmB$_6$. Further, we have carefully examined the spin chiralities of the Fermi surfaces to corroborate the topological insulating nature of SmB$_6$.

II. COMPUTATIONAL DETAILS AND THE STRUCTURAL RELAXATION

SmB$_6$ crystallizes in a cubic structure of CaB$_6$ type with space group $Pm\bar{3}m$ (No. 221) and the lattice constant of...
4.133 Å. We have investigated the electronic structures of bulk SmB₆ using both the DFT and the DMFT incorporating the spin-orbit coupling (SOC). We used the DFT+DMFT scheme [22], implemented based on WIEN2K [20]. Coulomb and exchange interaction parameters were set by 7.00 eV and 0.83 eV, respectively, which were chosen to describe the known f-state multiplet structures from XPS data properly. For the impurity solver of the DMFT, we used both the noncrossing approximation (NCA) and the one-crossing approximation (OCA) [22]. It has been well tested for f-electron systems that the OCA captures well the correlated nature of f electrons [23]. For SmB₆, we checked that the band structure of the OCA is quite similar to that of the OCA.

Details of the electronic structure calculations for slab geometries of SmB₆ are as follows. For the DFT, we used both the full-potential linearized augmented-plane-wave (FLAPW) band method implemented in WIEN2K [20] and the projector-augmented wave (PAW) band method implemented in VASP [21]. In both cases, we have employed the generalized gradient approximation (GGA) for the exchange-correlation potential. Bond lengths and internal atomic positions were optimized using the conjugate-gradient algorithm implemented in the VASP code until the residual forces were less than 0.01 eV/Å. For the plane-wave bases, the energy cutoff of 320 eV was used both VASP and WIEN2K to cross-check the density of states (DOS) and band structures. In WIEN2K calculations, wave functions inside the muffin-tin (MT) spheres were expanded in the spherical harmonics up to l_{max} = 10. The wave function in the interstitial region was expanded in the plane waves up to K_{max} \times R_{MT} = 7.0 (R_{MT} : MT radius). R_{MT}’s of Sm and B are chosen as 2.5 a.u. and 1.5 a.u., respectively. 24 × 24 × 2 k-point mesh was used in the Brillouin zone. To scrutinize the spin chirality of each Fermi surface originating from the surface states, the spin-noncollinear calculations were performed. To describe the surface states, two nonstoichiometric supercell geometries were employed, as shown in Figs. 1(a) and 1(b): (a) 9 Sm layers and 8 B₆ layers for the Sm-terminated slab, (b) 9 Sm layers and 10 B₆ layers for the B₆-terminated slab. In both cases, vacuum regions with 25 and 28 Å thickness, respectively, are considered in-between adjacent slabs. The resulting relaxed structures are shown in Figs. 1(a) and 1(b). In both cases, the slabs are seen to be shrink mainly within two topmost layers.

### III. RESULTS AND DISCUSSION

DMFT band structures in Fig. 2 demonstrate the temperature (T) dependent f-d hybridization behavior. At high T = 150 K in Fig. 2(b), Sm f electrons do not form coherent bands, and so the metallic Sm d band crossing E_F is clearly visible around X, reflecting little hybridization with incoherent f bands. Upon cooling, the f electrons form the coherent bands that become strongly hybridized with the d band so as to display a gap feature, even though the gap size is almost zero in the DMFT result of Fig. 2(a) (T = 5 K).

In Fig. 2(a), the DMFT bands are overlaid with DFT bands that are rescaled down in energy by 1/10 (thin dotted blue). It is seen that the DMFT and DFT band structures near E_F are essentially the same as each other. This feature suggests that the strong correlation effect of f electrons can be captured to some extent just by renormalizing DFT bands. The gap feature persists in the renormalized DFT band structure with a reduced size of ~2 meV with respect to the original gap size of ~20 meV. Of course, the renormalized DFT cannot simulate the Sm j = 7/2 bands that are to be shifted up by the strong correlation of Sm 4f electrons. So the position of Sm j = 7/2 bands in the DFT is located much closer to E_F than in the DMFT. In fact, the present authors have previously analyzed the influence of the low-lying Sm j = 7/2 bands on the states...
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The gap is seen to be realized between two bands, as shown in Figs. 3(b)–3(d). Namely, there are two more bands, as in Fig. 3(a). SmB6, however, shows a peculiar parity inversion feature. As discussed in Fig. 2, the occurrence of the gap in SmB6 is initiated by the f-d hybridization near X, but the band gap is seen to be realized between two f bands, as shown in Figs. 3(b)–3(d). Namely, there are two more f bands, β and γ, having the same negative parity (Xγ) in-between parity-inverted bands of α (Xα) and δ (Xδ). Therefore, some part of the surface in-gap states including the Dirac point would be buried in the bulk β and γ bands, as in Fig. 3(b). This feature in SmB6 is different from the usual topological insulators, in which the Dirac cone features are clearly observed in the gap region. This is an important difference, making SmB6 more complicated than other conventional topological insulators.

In order to probe into the surface states of SmB6, we have performed the DFT slab calculations for both Sm- and B6-terminated (001) surfaces, including Sm f electrons as valence electrons. Figures 4(a) and 4(b) show the surface states of Sm- and B6-terminated SmB6 slabs, respectively. In both cases, there appear metallic surface states in the bulk gap region, which are seen to merge into bulk bands projected to the surface BZ. The surface in-gap states here are composed of mainly the Sm f state (the weight of the f component is more than 90%). This result is quite contrary to the previous DFT surface band calculation [14], in which the surface states near EF came mostly from the B 2p dangling bond state. This discrepancy arises from that Sm f electrons were not taken into account as valence electrons in Ref. [14]. Without Sm f electrons, we also obtained the B 2p surface states that cross EF [26]. However, in this case, there are many other metallic bands near EF besides the B 2p surface bands due to the lack of hybridization with f electrons, which is certainly in disagreement with ARPES data. Note that the B 2p surface states do not satisfy the criterion of the topological insulator, whereas the present surface states including Sm f electrons do on both terminations. Thus the inclusion of f electrons as valence state changes the situation near EF dramatically.

At a glance, the surface states in Fig. 4(b) for the B6-terminated case look analogous to those obtained by the tight-binding (TB) surface model calculation based on the LDA+Gutzwiller bulk band result [11]. However, there are interesting differences. First, in the TB result, the gapless surface states, especially at X, seem to be generated from the band β manifesting the Dirac points in the gap region, while, in the present rescaled DFT, the Dirac point is seen to be just buried in the band β. This is not a minor distinction. Since the parities of bulk band β and γ are negative, the absence of both bands does not change the topological order. So the gapless surface states are not formed via the bulk band β and γ, but formed just passing through both bands [27]. Interestingly, a similar feature of a buried Dirac point in the bulk bands is also seen in PuB6, which was reported to be a correlated topological insulator [28].
Second, Sm-termination in Fig. 4(a) shows additional surface in-gap states centered at $M$, which have never been recognized theoretically. The existence of these metallic surface states does not violate the $E_F$ crossing criterion of $Z_2$ topological characterisation. The different surface states depending on the terminations are quite natural even in conventional topological insulators [29]. It is, however, rarely reported in real materials that additional metallic surface states emerge with different dispersions at another high symmetry point. Metallic surface states centered at $M$ have not been reported experimentally either. One reason why $M$-centered surface states have not been detected might be due to the fact that the size of a well-ordered $1 \times 1$ Sm-terminated surface known until now is not over a few nanometers [17,18]. The beam spot size of state-of-the-art ARPES may not be enough to capture the physics of such a small $1 \times 1$ ordered Sm-terminated surface.

Figures 4(c)–4(f) show the charge densities of surface wave functions at specific $k$ points. It is shown that the charge densities of the surface states originate indeed from the surface atoms, mainly from Sm atoms, of both terminated slabs. It is worthwhile to note in Fig. 4(c) that the surface state near $\bar{\Gamma}$ (A) is quite discernible from other surface states near $\bar{X}$ and $\bar{M}$ (B, C, D), in that the dominant charge density at A is slightly away from the topmost layer and locates rather close to the bulk side. This is also the case for the surface state at $\bar{\Gamma}$ for the Sm termination. This feature suggests that the surface state at $\bar{\Gamma}$ could be more robust than other surface states against any changes at the surface.

FIG. 4. (Color online) DFT band structures of SmB$_6$ slabs with (a) the Sm-terminated surface and (b) the B$_6$-terminated surface. Note that the energy scales in (a) and (b) are reduced by 1/10. Blue shaded region represents the projection of SmB$_6$ bulk bands to the (001) surface BZ. Red dots represent the crossing (Dirac) points of metallic surface bands. Insets show the total DOS divided by the number of Sm layers of each surface termination [25]. (c)–(f) Charge densities of wave functions at given points A, B, C, and D (green dots) of the metallic surface bands. (g), (h) Fermi surfaces of the Sm and the B terminations, respectively. Spin helicity in each Fermi surface is plotted with red arrow. (i) Dirac-cone-like shape of the spin chiral texture of the surface state at $M$. Charge densities in (c)–(f) are drawn based on the VASP data, while all the others are drawn based on the wien2k data.
STS/STM result. So the metallic surface states at \( \bar{M} \) can explain the larger differential conductance on the Sm-terminated surface.

Differently from \( \bar{\Gamma} \)- and \( \bar{X} \)-centered surface states in SmB\(_6\), \( \bar{M} \)-centered surface states, which emerge only in the Sm-terminated SmB\(_6\) for both VASP and WIEN2k band results, have not been explored in the context of topical insulators. In the topological insulators, Kramers degenerate pairs switch partners, reflecting the change in the time reversal polarization [30]. Also, the corresponding surface states cross the Fermi level (\( E_F \)) an odd number of times between TRIM (time reversal invariant momentum) points having different time reversal polarizations, \(-1 \) or \( 1 \). We checked the topological nature of the surface states at \( \bar{M} \). It is seen that the upper band at \( \bar{M} \) first increases in energy above \( E_F \) and then decreases down so as to be connected to the band (6) at \( \bar{\Gamma} \) below \( E_F \), while the lower band at \( \bar{M} \) is connected to the band (1) at \( \bar{\Gamma} \) above \( E_F \), as is schematically drawn in Fig. 5(b). It shows typical features of topological insulators such as “switching partners” and “an odd number of \( E_F \) crossing” [Fig. 5(c)], which is clearly different from that of normal band insulators [Fig. 5(d)]. But the Dirac cone at \( \bar{M} \) is seen to be reversed with respect to a normal Dirac cone in Fig. 5(c) that has monotonically decreasing or increasing dispersions.

To investigate the robustness of the Fermi surfaces, we examined the variation of the surface states with respect to a perturbation. For that purpose, we considered the situation that the top Sm layer of the Sm-terminated slab was shifted up from its equilibrium position by 0.5 \( \text{Å} \) [see Fig. 6(a)]. As shown in Figs. 6(b) and 6(c), due to this perturbation, two \( \bar{M} \)-centered Fermi surfaces disappear, while \( \bar{\Gamma} \)- and \( \bar{X} \)-centered Fermi surfaces are intact. The relevant surface states at \( \bar{M} \) become less dispersive and the Dirac point becomes lower than before. This feature suggests that \( \bar{M} \)-centered Fermi surfaces are likely to be more fragile than \( \bar{\Gamma} \)- and \( \bar{X} \)-centered Fermi surfaces. Note that these two \( \bar{M} \)-centered Fermi surfaces are not compulsory for the topological insulating nature of SmB\(_6\).

In our early investigation of bulk bands of SmB\(_6\) using the DFT [24], we found that Sm \( j = 7/2 \) bands above \( E_F \) are mixed somehow with the low-lying \( f \) bands near \( E_F \), so as to produce the spurious charge densities. Hence, to remove the influences of \( j = 7/2 \) bands around \( E_F \), we performed the slab calculations with the 10 times stronger SOC, as we did in the bulk case. We have ascertained that the overall features of metallic surface states, such as number of FSs, relative FS sizes, and the hole or electron nature of each FS, are almost unchanged even with the stronger SOC for both terminations. This result indicates that the effects of Sm \( j = 7/2 \) bands on the metallic surface states of SmB\(_6\) near \( E_F \) would be minor.

### IV. CONCLUSION

We have investigated the surface in-gap states of SmB\(_6\) based on first-principles DFT slab band structure analysis. We have found that (i) the surface states and corresponding FSs emerge at around \( \bar{\Gamma} \) and \( \bar{X} \), (ii) there appear additional
surface states centered at $\bar{M}$ for the Sm-termination case, and (iii) more importantly, the present surface states are quite different from those of existing surface band calculations, such as the TB slab calculation and the DFT calculation without considering Sm $4f$ electrons. We have also determined the spin helicities of Fermi surfaces, which are consistent with the topological Kondo insulating nature of SmB$_6$. For clear confirmation, spin-resolved ARPES on the ordered surface is strongly recommended.

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