Introduction.

Despite overwhelming evidence that dark matter (DM) is the dominant form of matter in the universe, we remain ignorant about its fundamental nature. An appealing class of DM candidates which enjoy considerable theoretical motivation are weakly interacting massive particles (WIMPs): heavy particles with weak-scale mass and interaction strengths. Indeed, the production of WIMP-type particles at the LHC is now one of the foremost goals of the particle physics community.

Given the large number of WIMP-type theories, it is desirable to express the DM interactions in a model-independent manner. This can be achieved with an effective field theory (EFT) framework, in which a set of non-renormalizable effective operators is used to parametrize the interaction of a pair of DM particles with Standard Model (SM) particles. The EFT operators would be obtained as a low energy approximation to a renormalizable theory by integrating out the particle(s) that mediates the interaction. A standard set of operators have been listed in Refs. [1,2] (see also [3]).

For fermionic dark matter $\chi$ interacting with SM fermions $f$, these operators take the form:

$$\frac{1}{\Lambda^2} (\Gamma_{\chi} \chi) (\Gamma_{f} f), \quad (1)$$

where $\Lambda$ has dimensions of mass and is related to the mass $M$ and coupling constants $g_i$ of a heavy mediator as $\Lambda = M/\sqrt{g_1 g_2}$, and $\Gamma_{\chi, f}$ are various Gamma matrices.

While the EFT description is very useful at low energies, such as those relevant for direct detection, it was long appreciated that the EFT approach may be unsuitable at LHC energies. Specifically, if the momentum transfer in a process is comparable to or larger than the mass of the mediator, the EFT will not provide an accurate description of the underlying physics. Many recent papers have attempted to quantify the point at which an EFT description is no longer valid [4-6] or have proposed the use of simplified models as an alternative framework for undertaking DM searches at colliders [7,10].

Here we make a more subtle point: if an EFT operator does not respect the weak gauge symmetries of the SM, it may be invalid at energies comparable to the electroweak scale, $v_{EW} \approx 246$ GeV, rather than the energy scale of new physics, $\Lambda$. For example, if we attempt to use electroweak gauge symmetry violating operators at LHC energies, serious difficulties can be encountered soon above the EW scale, such as the bad high energy behaviour of cross sections. An example is the well-known unitary violation rising as $s/(4 m_W^2)$ in $SU(2)_L$ non-invariant WW scattering, due to the longitudinal $W$ modes induced by the symmetry breaking. In the SM, the violations are removed by an internal Higgs particle, but internal fields are “integrated out” in the EFT formalism. Thus, the limit of validity for the operator is the weak scale if any internal Higgs or $W$ or $Z$ particle is present in the Feynman diagram. More generally, sacred symmetries like the electroweak Ward identity can be violated, which implies a weak-scale cutoff, as we explain later in this paper.

EFT Operators and Gauge Invariance.

The standard list of DM-SM effective operators [2] contains several operators which violate the SM weak gauge symmetries. We argue that if an EFT operator does not respect the weak gauge symmetries of the SM, it necessarily carries a pre-factor of the Higgs vev to some power, a remnant of the $SU(2)_L$ scalar doublet

$$\Phi \equiv \left( \phi^0 = \frac{1}{\sqrt{2}} (H + v_{EW} + i 3 \phi^0) \right). \quad (2)$$

Acting as an $SU(2)_L$ doublet, enough powers of $\Phi$ are required to form an $SU(2)_L$-invariant operator. The fields $\phi^\pm$ and $3\phi$ are gauged away to become, in unitary gauge, the longitudinal modes of the $W^\pm$ and $Z$. So, in fact, it is the real, neutral field $\frac{1}{\sqrt{2}} (H + v_{EW})$ whose $n^{th}$ power appears in the operator. Commonly, the $H$ part of the expression is omitted, leaving just an implicit $v_{EW}^n$ in the coefficient. Of course, the $v_{EW}^n$ must come with a $\Lambda^{-n}$. Omission of the $H$ part in the operator may ignore some interesting phenomenology. In this paper, we will also...
ignore the $H$ contributions to operators, and focus on the operators proportional to $(\frac{v_{EW}}{\Lambda})^\alpha$. Such terms in the coefficients of $SU(2)$-violating operators clearly satisfy the criterion that as $SU(2)$ symmetry is restored, $v_{EW} \to 0$, the operator’s coefficient vanishes, and the operator decouples.\footnote{In what follows, we will assume that there is but a single vev, $v_{EW}$. If there were further vevs, the good relation $m_H^2 = m_Z^2 \cos \theta_W$ requires the additional vevs to come from additional doublet fields, or to be be small if coming from non-doublet fields. The vevs then add in quadrature to give $2(m_W^2/\sqrt{2})$. Thus, any individual vev will offers an energy-scale below the SM vev. In the sense that we will argue against larger energy-scales for effective operators, our assumption of a single EW vev is conservative.}

**Scalar operator:** Consider the scalar (pseudo scalar) operators

$$\frac{m_q}{\Lambda^2} \langle \bar{q} q \rangle = \frac{m_q}{\Lambda^2} \langle \bar{q}_L q_R + h.c. \rangle. \quad (3)$$

This operator is clearly not $SU(2)_L$ invariant, as $\chi$ and $q_R$ are $SU(2)_L$ singlets, while $q_L$ is a vector (either $u_L$ or $d_L$) of the usual left-handed SM doublet, $Q_L$. A vector to the Higgs boson has been anticipated by the factor of $m_q$ in the coefficient. Most authors invoke minimal flavor violation to motivate this choice of normalization. Although this $SU(2)_L$ violating effective operator can be an attractive low energy description of new physics, notice that its coefficient cannot be arbitrarily large as it is controlled by the Higgs vev. Although formally a dimension 6 operator, it is competitive only with dimension 7 operators, given its $1/\Lambda^3$ normalization.

**Vector operator:** Now consider vector (or axial vector) operators of the form

$$\frac{1}{A^2} \langle \bar{q} q \rangle = \frac{1}{A^2} \langle \bar{q}_L q_R + h.c. \rangle. \quad (4)$$

These operators respect $SU(2)_L$ provided that the coefficients of the $u_L$ and $d_L$ operators are equal.\footnote{Isospin violating operators, such as those invoked in Ref.\cite{12}, can obviously be crafted from the RH quark fields.} Any ($\bar{q}_L q_L$) operator that does not have a matching $d_L$ term should be suppressed by two powers of $v_{EW}/\Lambda$ (one for each unmatched $u_L$):

$$\frac{v_{EW}^2}{\Lambda^2} \langle \bar{q} q \rangle = \frac{v_{EW}^2}{\Lambda^2} \langle \bar{q}_L | q_R \rangle. \quad (5)$$

Including the suppressed coefficient, this $SU(2)$-violating operator competes with dimension 8 operators, i.e., while the $SU(2)$ conserving (axial)vector operators are dimension 6, $SU(2)$ violating (axial)vector operators compete with subdominant, higher-order, dimension 8 operators.

**Mono-$W$ and $SU(2)_L$ invariance.**

Issues arise if one tries to use gauge symmetry violating operators at LHC energies. For particular processes, the lack of gauge invariance can manifest as a violation of unitarity in high energy scattering. As an example of a problem encountered with an $SU(2)_L$ violating EFT, consider the following operator:

$$\frac{1}{\Lambda^2} (\bar{q} \gamma^\mu q) (\bar{q} \mu u + \xi d \mu d). \quad (6)$$

This Lagrangian violates $SU(2)_L$, unless $\xi = 1$. The case of unequal $u$ and $d$ couplings was considered in Ref.\cite{13}, where a very strong constructive/destructive “interference effect” was found for $\xi = -1(+1)$, the degree of which depends on the energy scale. The analysis of Ref.\cite{13} was subsequently repeated by the LHC experimental collaborations ATLAS\cite{14} and CMS\cite{15,16}.

We shall demonstrate that the large cross section enhancement for $\xi \neq 1$ is in fact due the production of longitudinally polarized $W$’s as a result of breaking gauge invariance.

At parton level, the mono-$W$ process is $u(p_1)\bar{d}(p_2) \to \chi(k_3)\bar{v}(q)W^+(q)$. The relevant diagrams are given in Fig.\ref{fig:1} and the corresponding contributions to the amplitude $M = M^\alpha \epsilon^\alpha(q) = (M_1^\alpha + M_2^\alpha) \epsilon^\alpha(q)$ are

$$M_1^\alpha = \frac{1}{\Lambda^2} \left[ \bar{v}(p_2) \gamma^\alpha \gamma_5 \frac{g_W}{\sqrt{2}} \frac{P_L}{\sqrt{2}} u(p_1) \right] \left[ \bar{u}(k_3) \gamma_\mu v(k_2) \right],$$

$$M_2^\alpha = \frac{\xi}{\Lambda^2} \left[ \bar{v}(p_2) \gamma^\alpha \gamma_5 \frac{g_W}{\sqrt{2}} \frac{P_R}{\sqrt{2}} u(p_1) \right] \left[ \bar{u}(k_3) \gamma_\mu v(k_2) \right], \quad (7)$$

where $g_W$ is the weak coupling constant, and $\epsilon^\alpha$ is the polarization vector of the $W$. We note that the $W$ longitudinal polarization vector at high energy is

$$\epsilon^L_\alpha = \frac{q_\alpha}{m_W^2} + O(\frac{m_W}{E}) \sim \frac{s}{m_W^2}. \quad (8)$$

Thus the high energy $W_L$ contribution to the usual polarization sum, $\sum_\lambda \epsilon^L_\alpha \epsilon^L_\beta = -g_{\alpha\beta} + \frac{q_\alpha q_\beta}{m_W^2}$, is $\epsilon^L_\alpha \epsilon^L_\beta \approx q_\alpha q_\beta/m_W^2 \sim s/m_W^4$.

We can verify that the sum of the two amplitudes of Fig.\ref{fig:1} is not gauge invariant unless $\xi = 1$, by observing that the relevant Ward identity is not satisfied. At high energy, the Goldstone boson equivalence theorem requires that the amplitude for emission of a longitudinally

\begin{figure}[h]
\centering
\includegraphics[width=0.5\textwidth]{fig1.png}
\caption{Contributions to the mono-$W$ process $u(p_1)\bar{d}(p_2) \to \chi(k_3)\bar{v}(q)W^+(q)$, in the effective field theory framework.}
\end{figure}
polarized $W_L$ is equivalent to that for the emission of the corresponding Goldstone boson. Since the Goldstone boson couples to quarks with strength proportional to their mass, these terms are close to zero. (See Ref. [13] for a similar discussion about the related process $\chi\chi \to \nu eW$.) The Ward identity for the longitudinal $W$ at high energy therefore takes the form

$$M^\alpha e^\alpha_\xi \approx \frac{q_\alpha}{m_W} M^\alpha(q,...) = iM(\phi^+(q)) \simeq 0. \quad (9)$$

For the sum of the mono-$W$ amplitudes of Fig. 1 we find

$$q_\alpha M^\alpha = \frac{q_W}{s} \left[ \bar{u}(p_2) (1 - \xi) \gamma^\mu \frac{P_L}{\sqrt{2}} u(p_1) \right] \left[ \bar{u}(k_1) \gamma_\mu v(k_2) \right],$$

which clearly vanishes only for $\xi = 1$.

The “interference effect” seen in the mono-$W$ process is not truly due to constructive/destructive interference as previously claimed, but is just a manifestation of the fact that the breaking of electroweak gauge-invariance has given rise to a $W_L$ component. The increased cross section for $\xi \neq 1$ is in fact due to unphysical terms that grow like $s/m_W^2$, which originate from the $+g_q g_\beta/m_W^2$ term in the polarization sum. At high energy, these terms would grow large enough to violate unitarity. But even at lower energy, their presence may be problematic.

To explicitly demonstrate this behaviour, we now derive an analytic expression for the parton-level mono-$W$ process $d\sigma/dw e^+ e^- \to \chi\gamma$ we work in the center-of-mass frame, and follow the phase space parametrization described in Section V of Ref. [19]. We define $\theta$ to be the angle of the $W$ w.r.t. the beam line and $x = 2E_W/\sqrt{s}$, where $\sqrt{s}$ is the total invariant mass. For simplicity we take $m_\chi = 0$ (the cross section will be approximately independent of $m_\chi$ for $m_\chi^2 \ll s$). We include a factor of $1/3$ from averaging over initial state quark colors.

For $\xi = 1$ the differential cross section is well behaved and is given by

$$\frac{d^2\sigma}{dx d\cos\theta} \bigg|_{\xi = 1} = \frac{A}{3^2 2^8 \pi^3 A^4 \left( s^2 x^2 \sin^2 \theta + 2 s m_W^4 \cos(2\theta) - 2x + 1 \right) + 4m_W^4}^2,$$

where

$$A = s^2 g_W^2 \sqrt{x^2 - 4m_W^2/s} \left( 1 - x + \frac{m_W^2}{s} \right) \left[ s^3 x^2 \sin^2 \theta \left( \cos(2\theta) x^2 + 3x^2 - 8x + 8 \right) + 2s^2 m_W^2 \cos(4\theta) x^2 + 2 \cos(2\theta) \left( x^3 - x^2 - 4x + 4 \right) - 2x^3 + 17x^2 - 24x + 8 \right] - 4m_W^2 \cos(4\theta) + 2 \cos(2\theta) \left( x^2 + 4x - 8 \right) - 17x - 16m_W^6 \cos(2\theta) + 3 \right],$$

If we take the limit $m_W \to 0$, remove the color factor 1/3, and replace $g_W/\sqrt{s}$ with the electron charge $e$, we find Eq. (11) reproduces the cross section for the $e^+ e^- \to \chi\gamma$ monophoton process reported by Ref. [19] for $m_\chi = 0$ and unpolarized $e^+ e^-$ beams. This provides a useful check for our more complicated mono-$W$ calculation.

For $\xi \neq 1$, however, the cross section is not well behaved at high energy. The $+g_q g_\beta/m_W^4$ term in the polarization sum contributes to the cross section a term

$$\frac{d^2\sigma}{dx d\cos\theta} \bigg|_{q_\alpha q_\beta/m_W^2} = \frac{\left( \xi - 1 \right)^2 s^2 g_W^3 \sqrt{x^2 - 4m_W^2/x} \left( 2x^2 \sin^2 \theta - 16x + 16 + \frac{4m_W^4}{s} \cos(2\theta) + 3 \right)}{3^2 2^8 \pi^3 A^4 m_W^4}, \quad (12)$$

which violates unitarity when $s \gg m_W^2$.

The total cross sections, for $m_\chi = 0$, are plotted in Figs. [24] as a function of $\sqrt{s}$. We also calculate the cross sections in MadGraph [21], and find the results agree. For brevity of notation, we have defined $\sigma_1$ and $\sigma_2$ to be the contributions to the cross section from the $-g_q g_\beta$ and $+g_q g_\beta/m_W^2$ terms in the polarization sum, respectively. The $\xi = 0, -1$ cross sections grow faster with $\sqrt{s}$ than for $\xi = 1$. At LHC energies the cross sections are already dominated by the unphysical terms arising from the longitudinal polarization, unless $\xi \simeq 1$.

From Renormalizable Models to EFTs.

Let us now consider a renormalizable, gauge invariant, model of DM interactions, and examine the way in which unequal couplings to $u$ and $d$ quarks can be obtained. Consider the case where $\nu q \to \chi\gamma$ is mediated by the exchange of a $t$-channel scalar. The Lagrangian is given by

$$\mathcal{L}_{\text{int}} = \frac{1}{2} \frac{Q_L^* \nu_R^* \nu_R + h.c.}{m_W^2} = \frac{1}{2} \frac{Q_L^* \eta u_R^* + h.c.}{m_W^2} \chi_R + h.c., \quad (13)$$

where $Q_L = (u_L, d_L)^T$ is the quark doublet, $\eta = (\eta_u, \eta_d)^T \sim (3, 2, 1/3)$ is a scalar field that transforms
under the SM gauge group like $Q_L$, and $f$ is a coupling constant. Such couplings are present in supersymmetric (SUSY) models, with $\chi$ identified as a neutralino and $\eta$ a squark doublet, and have been considered as a simplified model for DM interactions in Refs. [22–25].

If we take the EFT limit, assuming the $\eta$ are very heavy, the lowest order operators are of dimension 6:

$$\frac{1}{\Lambda_x^2}(\bar{\tau}u)(\chi\Gamma \chi) \quad \text{and} \quad \frac{1}{\Lambda_x^2}(\bar{d}d')(\chi\Gamma \chi),$$

(14)

where the suppression scales are $\Lambda_{u,d} \propto m_{\eta_{u,d}}/f$. The relevant Lorentz structure $\Gamma$ is a sum of vector and axial vector terms as can be seen by Fierz transforming the $t$-channel matrix elements obtained from Eq.13 to $s$-channel form [26].

The strength of DM interactions with $u$ and $d$ quarks can differ if the masses of $\eta_u$ and $\eta_d$ are non-degenerate. However, given that $(\eta_u, \eta_d)$ form an electroweak doublet, their mass splitting must be controlled by $v_{EW}$. The relevant terms in the scalar potential are [27]

$$V = m_\eta^2 2(\Phi^\dagger \Phi) + 2\lambda_1 (\Phi^\dagger \Phi)^2 + m_\eta^2 (\eta^\dagger \eta) + \frac{1}{2} \lambda_2 (\eta^\dagger \eta)^2$$

$$+ \lambda_3 (\Phi^\dagger \Phi)(\eta^\dagger \eta) + \lambda_4 (\Phi^\dagger \eta)(\eta^\dagger \Phi).$$

(15)

If $m_\eta^2 < 0$ and $m_\eta^2 > 0$, the SM Higgs doublet obtains a non-zero vev, while the $\eta$ does not. The presence of $\lambda_4$ splits the $\eta$ masses as

$$m_{\eta_u}^2 = m_\eta^2 + (\lambda_3 + \lambda_4)v_{EW}^2,$$

(16)

$$m_{\eta_d}^2 = m_\eta^2 + \lambda_3 v_{EW}^2,$$

(17)

implying that $\delta m_\eta^2 = m_{\eta_d}^2 - m_{\eta_u}^2 = \lambda_4 v_{EW}^2$. Note that while we have engineered unequal scalar masses, and thus unequal DM couplings to $u$ and $d$ quarks, we do not have complete freedom. The parameter $\xi$ of Eq.6 is given by $\xi = 1/(1+\delta m_\eta^2/\Lambda^2) = 1/(1+\lambda_4 v_{EW}^2/\Lambda^2)$. For $\Lambda \gtrsim 1$ TeV and a perturbative value for $\lambda_4$, $\xi$ will not deviate far from 1. (Negative $\xi$ cannot be obtained from our renormalizable model.) Furthermore, it is clear that $SU(2)_L$ violating effects enter the EFT at order $v_{EW}/\Lambda^4$, i.e., the same order in $\Lambda$ as a dimension 8 operator.

In the renormalizable theory, the mono-$W$ process proceeds via the gauge invariant set of diagrams in Fig.4(a) and (b) map onto those in Fig.1(a) and (b) respectively. The diagram in Fig.4(c), in which the $W$ is

\footnote{In the good EW $SU(2)$ limit, the $\eta_u$ and $\eta_d$ are mass degenerate, and the massless $W^\pm$ emitted in diagram (c) establishes the validity of the EW Ward identity [28, 30]. When $EW SU(2)$ is broken, the $\eta_u$ and $\eta_d$ masses are split, and the new massive-$W$ longitudinal mode must restore the EW Ward identity by coupling to $\eta$ proportional to $\delta m_\eta^2$ [27]. This argument provides an interpretation of the result found earlier in [27] that the internal longitudinal mode couples proportional to $\delta m_\eta^2$. In fact, in [27] it was shown that this longitudinal $W$ mode will dominate the $W$ emission probability for some range of model parameters.}
radiated from the $\eta$, is suppressed by an additional heavy scalar propagator, and hence appears subdominant to the ISR diagrams. It enters the EFT as a dimension 8 operator, contributing on an equal footing with the $SU(2)$ violating contributions of diagrams (a) and (b) \[31\]. Finally, note that in the renormalizable theory, in the high energy limit, $W_L$ production arises solely from the amplitude of Fig.4(c), and only when $\delta m_\eta \neq 0$.

**Conclusion.**
An important observation of Ref.\[13\] is that, of the mono-$X$ processes, the mono-$W$ is unique in its ability to probe different DM couplings to $u$ and $d$ quarks. This important insight is correct. However, we have argued that the size of any $SU(2)_L$ violating difference of the $u$ and $d$ quark couplings must be protected by the EW scale, and therefore cannot be arbitrarily large. $SU(2)_L$ violating operators can be obtained by integrating out the SM Higgs or by including Higgs vev insertions. Therefore, they should have coefficients suppressed by powers of $(v_{EW}/\Lambda)$ or $(m_{fermion}/\Lambda)$ and thus are of higher order in $1/\Lambda$ than they would naively appear. To include $SU(2)$ violating effects in a way that is self consistent and properly respects the EW Ward identity, one should use a renormalizable, gauge invariant, model rather than an EFT, to avoid spurious $W_L$ contributions. These observations will be an important guide to the LHC collaborations in the interpretation of their current \[14–17\] and forthcoming mono-$W$ dark matter search results, and to theorists constructing EFTs.

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