In-plane quasi-single-domain BaTiO$_3$ via interfacial symmetry engineering

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The control of the in-plane domain evolution in ferroelectric thin films is not only critical to understanding ferroelectric phenomena but also to enabling functional device fabrication. However, in-plane polarized ferroelectric thin films typically exhibit complicated multi-domain states, not desirable for optoelectronic device performance. Here we report a strategy combining interfacial symmetry engineering and anisotropic strain to design single-domain, in-plane polarized ferroelectric BaTiO$_3$ thin films. Theoretical calculations predict the key role of the BaTiO$_3$/PrScO$_3$ (110)$_0$ substrate interfacial environment, where anisotropic strain, monoclinic distortions, and interfacial electrostatic potential stabilize a single-variant spontaneous polarization. A combination of scanning transmission electron microscopy, piezoresponse force microscopy, ferroelectric hysteresis loop measurements, and second harmonic generation measurements directly reveals the stabilization of the in-plane quasi-single-domain polarization state. This work offers design principles for engineering in-plane domains of ferroelectric oxide thin films, which is a prerequisite for high performance optoelectronic devices.

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Oxide interfaces have acquired much attention in the last decade due to the emergence of multifunctionalities. For example, LaAlO₃ and SrTiO₃ are both electrical insulators, but when they are grown on top of each other, highly conducting channels are formed at the interface, accompanying ferromagnetism and gate-tunable superconductivity. A key question that arises from such interfaces is whether bulk properties of a heterostructure can be controlled through the emergent states of matter at the interfaces. Interfacial effects arising from electrostatic and crystalline symmetry mismatches have been known to play important roles in determining the domain structures of ferroelectric thin films. Indeed, Yu et al. reported that atomically precise control of the interface could result in different polarization states in (001)-oriented ferroelectric films, having the polarization perpendicular to the surface. However, mechanisms underlying the interfacial symmetry mismatch on domain states and the ferroelectric response of in-plane polarized films are still not understood.

Single-domain in-plane polarized states are highly desirable for a number of potential functional device applications, such as high-performance electro-optic modulators and planar-type ferroelectric tunnel junctions. However, epitaxial oxide thin films with in-plane polarization typically exhibit complicated multi-domain states which can severely degrade optical device performances. For example, for ferroelectric waveguide applications, the waveguide loss and the electro-optic coefficient of ferroelectric materials are strongly influenced by the optical scattering by domain boundaries that exist in multidomain ferroelectric thin films and the crystalline quality of the films.

In this work, we report the strategy for in-plane single-domain in BaTiO₃ (BTO) ferroelectric thin films via interfacial symmetry and electrostatic potential mismatch using (110)ₖ-oriented PrScO₃ (PSO) substrates. Density functional theory calculations and phase-field simulations predict the key roles of the interfacial environment between a film and the substrate, i.e., anisotropic strain, monoclinic distortion, and interfacial electrostatic potential, in stabilizing in-plane single-domain in BTO films on PrScO₃ (PSO) (110)ₖ substrates. Scanning transmission electron microscopy (STEM), piezoresistive force microscopy (PFM), polarization hysteresis loop measurements, and optical second harmonic generation (SHG) results reveal that polarization direction of the BTO film is mainly along PSO [110]₀ direction, while it has a small variable tilting along PSO [002]₀ directions, leading to “quasi-single-domain” state. This work offers an approach to engineer in-plane ferroelectric epitaxial oxide thin films, enabling the development of device applications.

Results
Modeling of in-plane single-domain BTO. To design in-plane single-domain ferroelectric film, taking BTO—a canonical ferroelectric material—as a model system, we first discuss universal aspects of epitaxial strain for ferroelectric domain configurations. In general, in-plane polarization of ferroelectric oxide thin films is established under tensile strains. However, under an isotropic biaxial strain, such films typically possess complicated multi-domain structures due to the presence of two energetically degenerate ferroelastic variants, resulting in four possible ferroelectric variants (Fig. 1a). Even though a proper anisotropic strain could give rise to single in-plane ferroelastic variant, 180° ferroelectric domains, corresponding to two possible ferroelectric variants, are still energetically equivalent (Fig. 1b).

To energetically stabilize one of the two in-plane polarized states, we note that a symmetry lowering of the BTO film (i.e., monoclinic distortion) via an interfacial symmetry mismatch effect could play a central role (Fig. 1c). It is well known that interfacial oxygen octahedral coupling could initiate structures propagation over extensive distances and subsequently allows to tune the structure of epitaxial film. Once, at the interface between CaTiO₃ and NdGaO₃, oxygen octahedral coupling breaks the mirror symmetry and stabilizes a single domain structure with a single monoclinic tilt direction. Once a monoclinic distortion is introduced near the interface region, an out-of-plane polarization will appear due to the symmetry lowering and the orientation will be determined by the polarity of the substrate surface termination. Such a monoclinic distortion of BTO is likely to gradually relax as the thickness of the film increases, resulting in a single-domain in-plane ferroelectric state at the region far away from the interface (Fig. 1c).

To test feasibility of this approach, we consider orthorhombic rare-earth scandate (RescO₃) substrates (Supplementary Table 1). It should be noted that the pseudocubic (pc) lattice parameter of RescO₃ substrates, aₕ = 0.394 – 0.405 nm, is similar to c-lattice parameter of bulk tetragonal BTO (4.036 Å). In addition, (110)ₖ-oriented RescO₃ substrates possess a monoclinic nature since the out-of-plane direction ([110]₀) is not perpendicular to one of in-plane directions ([110]₀). Furthermore, a reliable method to obtain complete ScO₂-terminated RescO₃ has been reported. Among them, (110)ₖ-oriented RescO₃ substrates is a promising candidate for the following two reasons: first, its lattice parameters along bₜ (i.e., [002]₀) and cₜ (i.e., [110]₀) axis are similar to the b/c and c lattice parameters of bulk tetragonal BTO with misfit strains of +0.38% and –0.25%, respectively (Details in axis notations and the crystallographic relationship between BTO and PSO are represented in Supplementary Fig. 1). Second, PSO has a high in-plane anisotropic ratio (cₜ/bₜ) of 1.005, which is the largest among all scandates (Supplementary Table 1).

To evaluate the possibility of stabilizing an in-plane single-domain state in BTO/PSO heterostructures, we performed first-principles calculations. The BTO/PSO heterostructure was modeled using BTO lying on the top of ScO₂-terminated PSO [110]₀ (Fig. 2). Notably, we found that there is a monoclinic distortion in the BTO, and its tilt direction is opposite to that of PSO. Other possible structural configurations of BTO, where the tilt direction is the same as PSO, was also calculated (Supplementary Fig. 2a). Interestingly, BTO/PSO heterostructures with opposite tilt direction turn out to be energetically less favorable by 18.6 J/m² (For more details, see the Supplementary Fig. 2 and Note 1). As expected, the out-of-plane polarization component of BTO is pointed “downward” to the interface due to negative charges associated with the ScO₂-terminated PSO substrate, while the in-plane polarization component is preferably along PSO [110]₀ direction, resulting in an overall polarization along the diagonal direction. On the other hand, to predict possible ferroelectric domain structures far away from the interface of the BTO thin films, we employed the phase-field method. As suggested by the first-principles calculation, we assume that the initial state of the film has a uniform, in-plane polarization along PSO [110]₀ direction. The interfacial effect associated with the negative charges is considered by introducing a layered charge distribution at the interface. A more detailed description of the model is given in the Method section. A representative two-dimensional section of the phase-field simulation results demonstrate a quasi-single-domain polarization state in the in-plane direction along PSO [110]₀ as shown in Fig. 2b. There is also a spatial distribution of polarization which gradually rotates across the film thickness. Near the substrate-film interface an out-of-plane (toward the substrate) distorted polarization (Fig. 2d) is observed whereas near the film surface the polarization is entirely in-plane (along PSO [110]₀ direction) (Fig. 2c).
polarization gradually decreases through the film thickness while the in-plane polarization magnitude remains nearly constant. This single domain state with in-plane polarization in the BTO/PSO heterostructures is consistent with our model as shown in Fig. 1c, suggesting the possibility to stabilize such a unidirectional in-plane polar state.

Experimental demonstration of in-plane single-domain BTO.

For an experimental demonstration of BTO with single-domain in-plane polarization, BTO films with a thickness of 50 nm were grown on atomically smooth PSO (110)O substrates by pulsed laser deposition (PLD) (see “Methods” for details). The crystallinity of the BTO films on PSO substrates was inferred from four-circle X-ray diffraction (XRD) measurements with a Cu K$_{\alpha1}$ source (Supplementary Fig. 4). From reciprocal space maps of the BTO film around the PSO (332)$_{O}$ and PSO (240)$_{O}$ reflections, we concluded that the BTO films are fully coherent with the PSO substrate. The lattice parameters of BTO were determined to be
The substrate. Color bar represents the distribution of BTO (Fig. 3g) along PSO 110plane. Figure 3a shows low magnification scanning transmission electron microscopy (STEM) images of the BTO film along the PSO 002 zone-axis. Ti displacements are represented by arrows in Fig. 3b, c, e, f, where the size of the arrows corresponds to the magnitude of atomic displacement in each unit cell. The average value of the out-of-plane component of the Ti displacement in the middle region of the film is negligibly small (−0.6 ± 0.9 pm), while strong downward polarization near the interface region (−8.3 ± 1.0 pm) is observed (Fig. 3d). The result of a decreasing out-of-plane polarization towards the middle region of the film is consistent to phase field simulation results as shown in Fig. 2b–d. Remarkably, the BTO film has a unidirectional in-plane Ti displacement (Fig. 3g) along PSO 110plane direction in the middle region of the film (Fig. 3e) and BTO/PSO interface region (Fig. 3f). The average in-plane Ti-displacement for each region is estimated to be 6.0 ± 1.1 pm and 6.0 ± 1.0 pm, respectively, which is comparable to the Ti displacement along the polarization direction in bulk single crystal BTO39. The detailed overall polarization state of the BTO film is described in Supplementary Note 2. Furthermore, to verify the PSO (110)O substrate termination, atomic-resolution energy dispersive spectroscopy (EDS) elemental mapping was performed together with HAADF-STEM imaging at the BTO/PSO interface. Supplementary Fig. 7 clearly shows that the interface configuration is ScO2-BaO. It should be noted that the TEM data distinctly demonstrate that the polarization directions near the interface are downward (Fig. 3c, d), which is originated from the negative polarity of the substrate surface. Consistent results are obtained from the multiple spots of the sample, indicating that the surface of the PSO substrate is uniformly ScO2 terminated. This is not surprising, because after high-temperature annealing of rare-earth scandate substrates for sufficient time, ScO2 is known to be more stable than the corresponding rare-earth oxide at the surface27,30.

To directly observe the polarization configuration of a BTO film, high-angle annular dark-field (HAADF) imaging using scanning transmission electron microscopy (STEM) was employed. Figure 3a shows low magnification HAADF-STEM images of the BTO film along the PSO 002 zone-axis. Ti displacements are represented by arrows in Fig. 3b, c, e, f, where the size of the arrows corresponds to the magnitude of atomic displacement in each unit cell. The average value of the out-of-plane component of the Ti displacement in the middle region of the film is negligibly small (−0.6 ± 0.9 pm), while strong downward polarization near the interface region (−8.3 ± 1.0 pm) is observed (Fig. 3d). The result of a decreasing out-of-plane polarization towards the middle region of the film is consistent to phase field simulation results as shown in Fig. 2b–d. Remarkably, the BTO film has a unidirectional in-plane Ti displacement (Fig. 3g) along PSO 110plane direction in the middle region of the film (Fig. 3e) and BTO/PSO interface region (Fig. 3f). The average in-plane Ti-displacement for each region is estimated to be 6.0 ± 1.1 pm and 6.0 ± 1.0 pm, respectively, which is comparable to the Ti displacement along the polarization direction in bulk single crystal BTO39. The detailed overall polarization state of the BTO film is described in Supplementary Note 2. Furthermore, to verify the PSO (110)O substrate termination, atomic-resolution energy dispersive spectroscopy (EDS) elemental mapping was performed together with HAADF-STEM imaging at the BTO/PSO interface. Supplementary Fig. 7 clearly shows that the interface configuration is ScO2-BaO. It should be noted that the TEM data distinctly demonstrate that the polarization directions near the interface are downward (Fig. 3c, d), which is originated from the negative polarity of the substrate surface. Consistent results are obtained from the multiple spots of the sample, indicating that the surface of the PSO substrate is uniformly ScO2 terminated. This is not surprising, because after high-temperature annealing of rare-earth scandate substrates for sufficient time, ScO2 is known to be more stable than the corresponding rare-earth oxide at the surface27,30.

By ferroelectric polarization hysteresis measurements, we explored the as-grown polarization state of the BTO/PSO heterostructures. The schematics of the electrode configurations for in-plane polarization hysteresis measurements are shown in Fig. 4a. The measurements were performed along two directions: PSO 110plane and PSO 002plane. Notably, a well-defined hysteresis loop is observed only when applying electric field parallel to PSO 110plane, clearly showing the existence of ferroelectricity (Fig. 4b). The overall positive slope of the polarization in the field region from −30 to 30 kV cm−1 is attributed to the PSO substrate (Supplementary Fig. 8). The hysteresis loops are off-centered toward the negative field direction, pointing to a large polarization imprint mainly due to the asymmetric energy barrier between two polarization directions, i.e., PSO 110plane and PSO 110plane. The polarization signal obtained with electric field parallel to PSO 002plane direction reveals that there is no remanent ferroelectric polarization along this direction (Fig. 4c). However, the non-linear and weak hysteresis behavior of the P-E loops imply a possible polarization rotation along the PSO 002plane direction. The origin of this polarization rotation will be discussed later. From the STEM results, we found that the polarization...
direction of as-grown BTO is along PSO $[110]_0$. This is in good agreement with the observation that there is no hysteresis when we apply a positive electric field toward PSO $[110]_0$ since the polarization of BTO is already saturated in this direction in the as-grown state. Only under negative electric field a hysteresis loop is formed, indicating polarization reversal towards PSO $[110]_0$. It should be noted that when the field sweep is completed, the BTO film has its original polarization state, that is, a polarization towards PSO $[110]_0$ is still retained. This is a strong evidence for the in-plane polarization state toward PSO $[110]_0$ in our BTO samples is driven by the interfacial electrostatic potential which is not altered under bias conditions.

To better understand the microscopic domain structure, we performed angular-dependent lateral PFM measurements when the BTO film was rotated by a discreet angle with the respect to the surface normal (Fig. 5). As-grown BTO does not show any contrast in vertical PFM phase image mode (Supplementary Fig. 9). However, angular dependent lateral PFM measurements show that there are measurable domain features depending on the relative sample-cantilever orientation, where the lateral PFM signal is sensitive to the projected polarization along the axis perpendicular to the cantilever arm. Detailed analysis of the PFM images (Supplementary Fig. 10) reveals that the polarization is mainly along PSO $[110]_0$, consistent with the STEM results (Fig. 3g) and the polarization hysteresis measurements (Fig. 4a). However, there are small periodical zigzag-type changes in the polarization orientation typically within $\pm 15^\circ$ relative to PSO $[110]_0$ with respect to the PSO $[002]_0$ and $[002]_0$ directions resulting in a quasi-stripe domain structure with a lateral periodicity in the order of 50 nm and overall in-plane domain pattern (Fig. 5).

Fig. 3 STEM imaging and polarization measurements of BTO/PSO heterostructure. a A low-magnification HAADF-STEM image of the BTO film with a zone axis of PSO $[002]_0$. b, c High resolution images taken from selected areas (red and blue boxes in Fig. 3(a), respectively), shows out-of-plane component of Ti-displacement in the middle region (b), and near the interface region (c) of the BTO film, respectively. Note that the size of arrows corresponds to the amount of Ti-displacement. d Average value of out-of-plane Ti-displacement in each layer of BTO from the interface. e, f, High resolution images showing in-plane component of Ti-displacement in the middle region (e), and near the interface region (f) of the BTO film. g Average in-plane Ti-displacement in each layer of BTO from the interface. Both out-of-plane and in-plane Ti-displacements are extracted from the same regions in the BTO film. The error bars represent the 80% confidence intervals.

Fig. 4 In-plane polarization measurement versus electric field. a Schematics depicting parallel electrodes on the BTO/PSO sample. The 10-nm-thick SrRuO$_3$ patterns which are oriented along two different directions with 50-µm gap are used as electrodes for the measurements. b, c Room temperature hysteresis loop measurements for two parallel electrodes arrangements where the electric field is applied parallel to PSO $[110]_0$ (b), and PSO $[002]_0$ (c) directions, respectively.
and interpretation on the PFM imaging of domain structure along PSO (002)₀ are described in Supplementary Note 3.

Discussion
The presented data highlights that in-plane polarized single-domain BTO thin film is achievable by control of anisotropic strain, monoclinic distortion due to structural mismatch at an interface, and interfacial valence mismatching. Near the BTO/PSO interface, presence of both in-plane and out-of-plane polarization components result in a diagonal direction of polarization whereas the polarization of BTO in the middle region of the film is entirely in-plane (along PSO [110]₀). The out-of-plane polarization gradually decreases through the film thickness (Fig. 3d), while the in-plane polarization magnitude remains almost constant (Fig. 3g). This is fully consistent with structural analysis showing that the BTO films have slight monoclinic distortions towards the BTO [001]₀ direction (Supplementary Fig. 17), while there is no tilting along BTO [010]₀ direction (Supplementary Fig. 18). Such structural distortions are in accordance with the monoclinic symmetry probed by optical SHG measurements (Supplementary Figs. 20–22). From the local electron diffraction patterns, the monoclinic tilting angles between BTO [001]₀ and BTO [100]₀ near the interface region and film surface region are 91.11° and 90.58°, respectively (Supplementary Fig. 17e, f), indicating the structural relaxation far away from the interface, which is also confirmed by geometric phase analysis (GPA) from TEM data (Supplementary Note 4).

We now discuss the polarization rotation along the PSO (002)₀ direction. This is mainly due to the absence of a suitable single crystal substrate which has the same b (=a) and c lattice parameters of bulk tetragonal BTO. Tensile strain along the PSO (002)₀ as shown in Supplementary Table 1 could give rise to such a non-zero polarization state, leading to the zigzag-type as-grown domain structure (Fig. 5f). The polarization rotation in as-grown state results in non-linear and weak hysteresis behavior in P-E loop with applying electric field along the PSO [002]₀ direction (Fig. 4c). The origin of non-zero polarization along the PSO [002]₀ direction is further supported by phase field simulation where pure in-plane single-domain state is achieved by simply eliminating tensile strain along the PSO [002]₀ direction (Supplementary Figs. 13–15). Therefore, we concluded that the strategy presented in this work effectively stabilizes single ferroelectric variant along the PSO [110]₀ direction, even though unavoidable extra variants still exist (Fig. 5g).

The strategy we present here is to utilize a structural mismatch and the effect of an out-of-plane parameter (electric field) to manipulate the in-plane properties (polarization) by lowering the symmetry. We have experimentally demonstrated this strategy by preparation of BTO thin films on PSO (110)₀ substrates where quasi-single-domain state along PSO [110]₀ direction is achieved at room temperature. We anticipate our strategy for reducing undesirable variants also to be generally used for tuning in-plane properties of correlated materials where their emergent states are subject to domain evolutions.

Methods
Sample growth and characterization. The BTO films were grown on (110)₀-oriented PSO substrates by PLD with in-situ reflection high-energy electron diffraction (RHEED) monitoring (Supplementary Fig. 4a). The BTO ceramic target was ablated using a KrF (248 nm) excimer laser at a repetition rate of 3 Hz with the laser fluence of ~2 J/cm². The substrate temperature was kept at 680 °C with an oxygen partial pressure of 120 mTorr during the growth. The substrate-to-target distance was 60 mm. In all experiments, (110)₀-oriented PSO substrates provided by CrysTec with miscut angles of ~0.1° were used. The PSO substrates were soaked in deionized water for 30 min, and then annealed at 1100 °C in an oxygen atmosphere for 3 h.

DFT calculations. Density functional theory calculations were performed using the projector augmented plane-wave method and the Perdew-Burke-Ernzerhof exchange-correlation functional. The projector augmented plane-wave method and the Perdew-Burke-Ernzerhof exchange-correlation functional were used in all calculations. The basis set was comprised of a scalar relativistic spin-polarized all-electron Troullier-Martins-type pseudopotential for Ba, Ti, O, and TM atoms. The valence electron wave functions were expanded in a plane-wave basis set with a kinetic energy cutoff of 340 eV. The exchange-correlation functional was described in terms of the generalized gradient approximation. The energy cutoff for the plane-wave basis set was set to 400 eV. The Monkhorst-Pack k-point mesh was used to sample the Brillouin zone. The electronic self-consistent field iteration was stopped when the change in total energy was less than 10⁻⁵ eV. The force tolerance was set to 0.02 eV/Å. The structural optimization was performed using the conjugate gradient method. The relaxation was considered converged when the force on each atom was less than 0.01 eV/Å. The structural optimization was performed using the conjugate gradient method. The relaxation was considered converged when the force on each atom was less than 0.01 eV/Å. The relaxed structures were found to be local energy minima by analyzing the second-order force constants with the analytic Hessian matrix. The electronic properties were calculated using theDirac tensor formalism. The electronic band structures and density of states were calculated using the Dirac tensor formalism. The electronic band structures and density of states were calculated using the Dirac tensor formalism.
exchange-correlation functional\(^3\) as implemented in the Vienna ab-initio simulation package (VASP)\(^3,4\). A bilayer structure was employed in the calculations with a ferroelectric (100) BTO layer lying on top of an orthorhombic (110) PSO layer. The theoretical lattice constants of bulk PSO: \(a = 5.73 \text{ Å, } b = 5.75 \text{ Å, } c = 8.13 \text{ Å}\). We used a fixed atomic coordinate of first three layers of PSO to their bulk values and relaxed the rest consisting of one and half layer of PSO and eight layers of BTO (Fig. S2) with the energy convergence limit of \(1 \times 10^{-8} \text{ eV}\). In the calculations, a kinetic cutoff energy of 340 eV was used for plane wave expansion and a \(4 \times 4 \times 4\) Monkhorst-Pack grid\(^5\) of k points was used for Brillouin zone integration.

**Phase-field simulations.** In the phase-field model, imposed misfit strain is calculated to be anisotropic by using the pseudocubic lattice constants between BTO and PSO. The system is relaxed to reach an equilibrium state by evolving the polarization configuration with the time-dependent Ginzburg-Landau equation\(^8\).

The ferroelectric BTO is described by the spatial distribution of the spontaneous polarization \(P(x,y,z)\), the relaxational kinetics of which follows the time-dependent Ginzburg-Landau equation,

\[
\Delta \frac{\delta F}{\delta P} = -\frac{\delta F}{\delta P}
\]

(1)

Here, \(F\) is the free energy which consists of elastic \((f_{\text{elastic}})\), electrostatic \((f_{\text{electrostatic}})\), bulk \((f_{\text{bulk}})\), and gradient \((f_{\text{gradient}})\) energy contributions, and \(L\) is the kinetic coefficient.

The total free energy can be expressed as,

\[
F = f_{\text{bulk}} + f_{\text{elastic}} + f_{\text{electrostatic}} + f_{\text{gradient}}\mu\text{V}
\]

(2)

More in-depth description of each term in the energy contributions can be found in the references\(^6\). The parameters of the model for BTO follows from Li et al.\(^5\).

The 3D system is discretized into a 128\(\times\)128\(\times\)\(\Delta\) grid with \(\Delta x = \Delta y = \Delta z = 1 \text{ nm}\). The thickness of the substrate takes up \(30\Delta z\) to accommodate the relaxation of the displacement arising from the domain structure of the 50 nm film. The free surface of the film is described by the traction-free boundary condition on the top while the bottom interface is assumed to be fully coherent. As a result, the prescribed misfit strains between the film and the substrate can be calculated by using the pseudocubic lattice constant \(d_{\text{BTO}}^{\text{psic}} = \left(\frac{d_{\text{BTO}}^{\text{BTO}}}{d_{\text{BTO}}^{\text{BTO}}\text{STO}}\right)^2\) of BTO and that of the (110)\(_3\) plane of PSO, i.e., \(e_{\text{psic}} = \frac{d_{\text{BTO}}^{\text{psic}} - d_{\text{BTO}}^{\text{BTO}}}{d_{\text{BTO}}^{\text{BTO}} - d_{\text{BTO}}^{\text{STO}}} = 0.506\%\) and \(e_{\text{psic}} = \frac{d_{\text{BTO}}^{\text{psic}} - d_{\text{BTO}}^{\text{BTO}}}{d_{\text{BTO}}^{\text{BTO}} - d_{\text{BTO}}^{\text{STO}}} = 0.011\%\). As the lattices of the film and the substrate on the interface are orthogonal, there is no in-plane shear misfit strain, i.e., \(e_y = e_z = 0\%\). Considering the absence of top and bottom electrodes of the BTO film in experiments, we adopt the open-circuit boundary condition at both top and bottom of the film, i.e., \(D = n = 0\), where \(D\) is the electric displacement and \(n\) is the normal of the interface plane. The elastic and electric equilibrium equations for the thin-film system are solved following the method developed by Li et al.\(^5\).

To account for the interfacial effect as predicted by the first-principles calculations, we assume an effective charged layer at the bottom interface with a thickness of \(0.5\text{ nm}\) behind a band pass filter. Theoretical analysis is based on GPA\(^3\) that is preinstalled in Gatan Digital Micrograph software.

**Data availability**

The data that support the findings of this study are available from the corresponding author on reasonable request.

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Author contributions
C.B.E., E.Y.T., L.Q.C., A.G., Q.X.P., V.G. and T.T. supervised the experiments. K.E., J.W.L., S.R., H. Lee and T.H.K. performed the sample growth and surface/structural characterizations. T.R.P. and E.Y.T. performed DFT calculations. B.W., J.A.Z. and L.Q.C. carried out phase field simulations. H.Lu and A.G. performed PFM measurements. H.X.H., W.P.G. and X.Q.P. carried out STEM measurements. S.L., K.E., J.W.L. and S.R. performed the device fabrication and ferroelectric measurements. Y.Y., S.L. and V.G. performed SHG measurements and analysis.

Competing interests
The code used to produce the phase-field simulation results is licensed to Mu-PRO LLC, of which is owned by L.Q.C. All other authors declare that they have no competing interests.

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