Probing the limits of gate-based charge sensing

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Quantum computation requires a qubit-specific measurement capability to readout the final state of individual qubits. Promising solid-state architectures use external readout electrometers but these can be replaced by a more compact readout element, an *in situ* gate sensor. Gate-sensing couples the qubit to a resonant circuit via a gate and probes the qubit’s radiofrequency polarizability. Here we investigate the ultimate performance of such a resonant readout scheme and the noise sources that limit its operation. We find a charge sensitivity of \(37 \mu eH \text{ Hz}^{-\frac{1}{2}}\), the best value reported for this technique, using the example of a gate sensor strongly coupled to a double quantum dot at the corner states of a silicon nanowire transistor. We discuss the experimental factors limiting gate detection and highlight ways to optimize its sensitivity. In total, resonant gate-based readout has advantages over external electrometers both in terms of reduction of circuit elements as well as absolute charge sensitivity.

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High-fidelity quantum state readout is a requirement for the implementation of a quantum computer. In semiconductor architectures, readout is typically performed via a separate, proximal charge sensor, in contrast to in situ gate-based readout. To date, the most sensitive electrometers are the radiofrequency quantum point contact (r-QPC) and the radiofrequency single-electron transistor (r-SET)3-7, providing charge sensitivities at the μeHz−1/2 level8-10. However, the integration of these detectors adds additional elements to the architecture, complicating scalability.

Circuit quantum electrodynamics describes an alternative method to readout the state of a quantum system. The self-resonance of a high-frequency resonator is modified by the state-dependent polarizability of the quantum systems coupled to it. It allows readout via the dispersive and dissipative interaction between resonator and qubit. This technique has been demonstrated for superconducting qubits11-14 and semiconductor charge15,16 and spin qubits17,18. Outside the strong coupling limit of circuit quantum electrodynamics, resonant LC circuits have been coupled directly to the ohmic contacts of double quantum dots to readout their charge and spin states19,20, and to determine their complex admittance21. Furthermore, it has recently been demonstrated that the gates defining these quantum systems can also act as fast and sensitive readout elements, using the state-dependent polarizability as detection mechanism1.

While the high-frequency polarizability of quantum systems is well understood in terms of Sisyphus resistance22, and state-dependent quantum or tunnelling capacitance22-25, the sensitivity of gate detection has only been reported at the μeHz−1/2 range for GaAs19,26. In other semiconductor materials, charge and spin readout have been achieved27-32 and fast detectors have been demonstrated33-35 but little progress has been made towards gate-based sensing36. More generally, the noise inherent to any fast-driven two-level system, akin to the cyclostationary noise37 that the sensitivity is limited by a type of noise, which we call Sisyphus noise, that couples to the resonator’s natural frequency of oscillation. We use our model to determine the ultimate charge and phase sensitivity of gate-based detectors and predict that the latter have the potential to outperform r-SETs.

Results

Device and measurement technique. The device used here is a narrow channel silicon-on-insulator (SOI) nanowire transistor. A polycrystalline silicon top gate (length l = 64 nm) wraps around three faces of the nanowire and is separated from the channel (width w = 30 nm) by an oxide of 1.3 nm equivalent thickness offering a strong control over the channel electrostatics. The electric field exerted by the gate is strongest at the top most corners, where two gate faces meet. Owing to this so-called corner effect, electron accumulation in silicon NWFETs38 happens first at the top most corners. In addition, potential irregularities along the transport direction39,40 confuse these corner channels creating a parallel double quantum dot as schematically displayed in Fig. 1a. We couple the double-dot to a resonant LC circuit via the top gate electrode as depicted in Fig. 1b and measure the reflected radiofrequency signal6,19,41. At the resonant frequency (f0 = 1/2π√LC0 = 334.8 MHz, C0 is the detector’s stray capacitance) the magnitude (γ) and phase (φ) components of the reflected signal are sensitive to admittance changes of the

Figure 1 | Device and measurement set-up. (a) Sketch of the cross-section of the device perpendicular to the transport direction. Owing to the corner effect in silicon nanowire FETs and potential irregularities, a parallel few-electron double quantum dot system forms when Vg is biased just below threshold. (b) Electron micrograph of an equivalent device (l = 64 nm, w = 30 nm) embedded in a resonant tank circuit. C0 is the parasitic capacitance to ground and L a surface mount inductor. Vsd, Vg and Vbg are the DC voltages applied to the source, top gate and back gate, respectively. (c) Characterization of the reflectometry response in magnitude (top frame) and phase (bottom frame) for the OFF (Vsd = 0 V) and ON (Vsd = 1 V) state of the transistor. (d) Top panel: energy band diagram as a function of reduced gate voltage ng. The initial detuning position is set by r0 and Δν is the amplitude of the RF excitation. Γc, (→) represents the tunnelling into (out of) the dot. Bottom panel: 3D–0D tunnel rates as a function of ng calculated for €e = 15 meV and T = 100 mK.

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device (Fig. 1c). Changes in the power dissipation in the system are captured in $\gamma$, whereas $\phi$ reflects susceptance changes because of tunnelling or quantum capacitance$^{1,21,24}$. The origin of the gate-sensor signal can be understood in terms of electronic transitions in a fast-driven tunnel-coupled two-level system$^{24}$. Here we consider inelastic charge tunnelling between the quantum dots and the leads. The levels $E_0$ (dot empty) and $E_1$ (dot full) are aligned at $n_g = 0.5$ as shown in Fig. 1d. The system is driven cyclically around a DC bias point $n_g^0 = C_g V_{g0}/e$ with frequency $f_0$ comparable to the tunnel rate and amplitude $\delta n_g = C_g V_{g0}^f/e$. Here $C_g$ is the gate capacitance and $V_g$ and $V_d$ are the DC and RF gate voltage, respectively. Starting from the ground state at $n_g^0$, the fast RF excitation $\delta n_g$ moves the system out of equilibrium to the right of the degeneracy point. The system is now in the excited state until it inelastically tunnels. The excess dissipated energy $\Delta E = E_1 - E_0$ is then captured as a change in the total reflected power of the device. The dispersive signal may be detected when electrons on average tunnel out-of-phase with the rf cycle, generating an additional tunnelling capacitance contribution $C_t = x\delta(n_e)/\partial V_g$, where $\delta(n_e)$ is the average charge in the island.

The mechanism has previously been studied in the context of Sisyphus dissipation for three-dimensional (3D) metallic islands$^{24,42}$. Here we transfer the concept to confined systems with a 0D density of states coupled to 3D electron reservoirs. The corresponding tunnel rates are shown in the lower panel of Fig. 1d. A Fermi’s golden rule calculation yields the 3D-0D tunnel rates,

$$\Gamma _ \pm = \frac{\Gamma_0}{1 + e^{\pm\Delta E/\kappa_0 T}}$$

where $k_0$ is the Boltzmann constant, $T$ the temperature, $\Delta E(t) = E_1(1 - 2n_g(t))$ the time-dependent energy difference and $n_g(t) = n_g^0 + \delta n_g \sin(2\pi f_0 t)$ is the normalized gate voltage. $\Gamma_0$ is the constant tunnel rate that establishes away from the degeneracy.

In order to evaluate the performance of the gate sensor we first compare the results to standard direct current measurements. Fig. 2a shows the characteristic Coulomb diamonds where the electron occupancy is well defined. The onset of current happens at the diagonal lines marked by the green and red arrows indicating the alignment of the electrochemical levels of QD1 to the source and drain reservoirs, respectively (see Fig. 2b). Moreover, we observe a shift of the high-current regions at the orange lines, which can be understood as a capacitive shift of the QD1 transport characteristics because of the loading of an electron on QD2. However, QD2 is only coupled to the source reservoir as depicted in Fig. 2b and cannot be measured in transport.

The magnitude response of the gate sensor in the same voltage region as the DC transport experiment is presented in Fig. 2c. The signal outlines the edges of the charge-stable regions previously observed in the DC transport measurements. An important difference between the DC and RF measurements is observed, for example, at the QD2 charge transitions (orange arrows). The gate sensor magnitude response is enhanced when the electrochemical levels of dot QD2 and the source reservoir are aligned, demonstrating the possibility to detect charge transitions without the need of current flow or external charge sensors. The detector maintains its sensitivity at high $V_{sd}$ as opposed to what is observed in 3D charge islands$^{24}$. This additional feature stems from the independence of $\Gamma \pm$ on $V_g$ (equation 1).

In Fig. 2d we extract the dispersive contributions by analysing the phase response of the sensor. A change in the effective capacitance of the system because of electron tunnelling modifies the resonator’s resonant frequency and hence causes a phase shift at the sampling frequency ($f_0$). The phase response relates to an effective change in the capacitance, $\Delta C$, of the system given by $\Delta \phi \approx -\pi QAC/g_0$, where $Q$ is the quality factor of the resonator. Analogously to the magnitude response, we observe this phase shift $\Delta \phi$ at the edges of the conductive regions demonstrating dispersive readout of the charge state of a few-electron quantum dot system. Phase changes of the order of 1 mrad are easily resolved, translating into capacitance detection of $\sim 1$ aF, smaller than the $\sim$1 fF quantum capacitance of strongly coupled quantum systems$^{25}$.

Figure 2 | DC/RF readout comparison. (a) Source-drain current $I_{sd}$ as a function of $V_g$ and $V_{sd}$ for $V_{sd} = 2.4$ V. The numbers $(n,m)$ indicate the electron occupancy in in QD1 (n) and QD2 (m). The coloured arrows point to the onset of the transitions depicted in b. (b) Schematic diagram of a top view of the double-dot configuration. QD1 is tunnel-coupled to the drain (source) indicated by the magenta (green) arrows, while QD2 is only coupled to the source (orange arrow). Gate sensor magnitude response $\Delta \gamma$ (c) and phase response $\Delta \phi$ (d) in the same bias region as a. Arrows indicate the same transitions as in a.
Experimental charge sensitivity. We now move on to the experimental characterization of the gate sensor’s charge sensitivity. In Fig. 3a we show a typical transfer curve $\Delta V_g - V_g$ showing two electron transitions. $V_g = 0.5125$ V is the first electron on QD2 and $V_g = 0.5157$ V is the first electron on QD2. Inset (i) Sidebands at the point of maximum transconductance ($V_g = 0.5155$ V) at 20 kHz and equivalent excitation amplitude of 0.01 e (solid black line) and fitted curve (dashed orange line). The measurement bandwidth is $B_{SA} = 1$ kHz. Charge sensitivity as a function of carrier frequency (b) and carrier power (c). The 3-dB bandwidth, equivalent to 8 MHz, is indicated by the blue arrow. (d) Top panel: source-drain current ($I_{sd}$) as a function of source-drain voltage $V_{sd}$ through a blockaded region at $V_g = 0.58$ V. Bottom panel: noise temperature as a function of source-drain voltage measured at the resonant frequency with a resolution bandwidth of 1 MHz (red solid line). No rf excitation is applied during this measurement. The grey band indicates the calibrated noise temperature of the cryogenic amplifier, $T_N = 7.5 \pm 0.2$ K.

The sensitivity of rf-SETs is limited by shot noise because of the stochastic nature of the current through the tunnel barriers.\(^4\) Similarly, resonant readout techniques are in theory limited in their sensitivity by the noise that arises because of the fast drive exerted on the system. A discussion of this type of cyclostationary noise follows in the next section. Here we discuss external factors limiting the gate sensor performance. In Fig. 3d we experimentally characterize the noise temperature of the system at the resonant frequency as a function of $V_{sd}$. The top panel shows the source-drain current across a Coulomb blockade region; the bottom panel displays the system’s noise temperature, $T_N$, in the same region. $T_N$ remains constant independent of the device’s current level and coincides with the noise temperature of the cryogenic amplifier, 7.5 ± 0.2 K highlighted in grey (The amplifier noise was calibrated using shot noise thermometry according to ref. 46.). We conclude that the noise, and hence also the sensitivity of the gated-based charge sensor presented here, is experimentally limited by the noise level of the first amplification stage and is independent of $I_{sd}$ as opposed to shot-noise-limited rf-SET detectors.\(^5,47\)

Furthermore, degradation of the detector’s sensitivity can arise from external sources of dissipation such as losses in the resonator components. We model these effects using an equivalent lumped-element circuit (see Fig. 3e,f) consisting of the device’s typical Sisyphus resistance ($R_{Si} = 300$ kΩ), the equivalent series resistance of the inductor ($R_s = 5.2$ Ω) and the equivalent dielectric loss ($R_d = 16$ kΩ) because of losses in the PCB board and the geometrical capacitance of the device (see Supplementary Fig. 1 and Supplementary Note 1). Losses because of the inductor account for a detrimental 10% on sensitivity, which could be improved by the use of a superconducting on-chip inductor. Dielectric losses account for 67% reduction, which could be alleviated by using lower loss PCB boards and optimizing the sample geometry to minimize the parasitic geometrical capacitance. For a lossless circuit as shown in

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**Figure 3** | Gate readout benchmark. (a) Typical transfer curve $\Delta V_g - V_g$ showing two electron transitions. $V_g = 0.5125$ V is the first electron on QD1 and $V_g = 0.5157$ V is the first electron on QD2. Inset (i) Sidebands at the point of maximum transconductance ($V_g = 0.5155$ V) at 20 kHz and equivalent excitation amplitude of 0.01 e (solid black line) and fitted curve (dashed orange line). The measurement bandwidth is $B_{SA} = 1$ kHz. Charge sensitivity as a function of carrier frequency (b) and carrier power (c). The 3-dB bandwidth, equivalent to 8 MHz, is indicated by the blue arrow. (d) Top panel: source-drain current ($I_{sd}$) as a function of source-drain voltage $V_{sd}$ through a blockaded region at $V_g = 0.58$ V. Bottom panel: noise temperature as a function of source-drain voltage measured at the resonant frequency with a resolution bandwidth of 1 MHz (red solid line). No rf excitation is applied during this measurement. The grey band indicates the calibrated noise temperature of the cryogenic amplifier, $T_N = 7.5 \pm 0.2$ K. Lossy (e) and lossy (f) impedance matching circuits. $R_{Si}$ is the Sisyphus resistance of the device, $R_s$ is the inductor equivalent series resistance and $R_d$ is the equivalent dielectric loss of the resonator.
Fig. 3e, we predict that the measured sensitivity could be lowered to $10 \, \mu\text{e}\text{Hz}^{-\frac{1}{2}}$.

Finally, an improvement of $\delta q$ could be achieved if the resonant circuit were designed to match the high Sisyphus impedance of the device, for example, using superconducting transmission lines to make a stub matching network.$^{49}$ We estimate that using this technique a minimum charge sensitivity of $0.9 \, \mu\text{e}\text{Hz}^{-\frac{1}{2}}$ could be achieved.

**Sisyphus model and comparison to experiment.** We now turn to a theoretical description of resonant charge readout. It is substantially different from rf-SETs where the largest contribution to the reflected power comes from the modulation of its differential conductance. In resonant readout schemes single-electron tunneling is directly coupled to the frequency of the rf-drive and therefore a frequency-dependent noise spectrum is expected. To calculate the fundamental noise that limits resonant charge detection we develop a model of the correlation of the power and phase fluctuations in a fast-driven two-level system. In the following we neglect the back action of photon shot noise since our coupled resonator-qubit system is in the weak-coupling regime.$^{49}$

We first consider the dissipative components associated with fast electronic transitions. We present in the following a numerical calculation of the instantaneous dissipated power, $P(t)$, due to the rf excitation, the corresponding spectral density of the fluctuations in dissipative power, $S_{pp}$, and the charge sensitivity, $\delta q$, using experimental parameters obtained earlier.

The dynamics of power dissipation are given by a master equation$^{42}$. For the 0D–3D tunnel rates (equation (1)) it reduces to solving the differential equation,

$$P_1(t) + \Gamma_0 P_1(t) = \Gamma + (t)$$

where $P_1$ is the probability of the electron being in the dot. Solving equation (2) for $P_1(t)$ we obtain the instantaneous dissipated power

$$P(t) = \Delta E(t) [\Gamma_0 P_1(t) + \Gamma + (t)]$$

as well as its average, $\langle P \rangle$, over one period $f_0^{-1}$, which is shown in Fig. 4a as a function of DC offset $n^0_g$. It is displayed for several tunnel rates, using the optimal RF excitation $\delta n = 0.03$. The most power is dissipated when the system is biased at the charge instability and no dissipation occurs for $n^0_g = 0.5 \gtrsim \delta n_g$ as expected. The change in average power dissipation, $d\langle P \rangle / dn_g^0$, is maximum at $n^0_g = n^0_{g,\text{max}} \approx n^0_g + \delta n_g$. With respect to tunnel rates, $\langle P \rangle$ peaks at $\Gamma_0 = 2\pi f_0$ showing a way to maximize the detector response. This can be understood from the analytical approximation given in equation (4), where $\Gamma$ is expanded around $n^0_g$ to the first order of $\delta n_g$.

$$\langle P \rangle \approx \left( \frac{eV^2}{2k_B T} \right)^2 \frac{1}{\cosh^2 \left( \frac{\Delta E(n^0_g)}{2k_B T} \right)} + \frac{\Gamma_0}{\Gamma_0 + \omega_0 / \delta n_g}$$

Note that this approximation is only valid for excitations $\delta n_g \ll k_B T / e \omega_0$. The numerical solution $P_1(t)$ of equation (2) (see Supplementary Note 3), furthermore, allows us to calculate the power fluctuations around the mean value and subsequently their power spectral density, $S_{pp}$ (see Supplementary Note 2). The results are shown in Fig. 4b as a function of reduced frequency $\pi f_0$ for several $\Gamma_0$ at $n^0_g = n^0_{g,\text{max}}$. At the point of maximum sensitivity the power noise is maximum at frequencies that match the excitation frequency $f_0$ and its harmonics. As a whole, these calculations show a new type of frequency-periodic noise, the Sisyphus noise, in which the stochastic nature of electron tunneling is directly coupled to the resonator’s natural frequency of oscillation. However, signal and noise frequency decoupling could be achieved at the degeneracy point $n^0_g = 0.5$ (See Supplementary Fig. 2).

Knowledge of the Sisyphus noise and the change in average power dissipation allows us now to calculate the charge sensitivity $\delta q = \frac{\sqrt{S_{pp}(\omega) / dP_1(t) / dn^0_g}}{dP_1(t) / dn_g^0}$

in units of $e \text{Hz}^{-\frac{1}{2}}$. The result is presented in Fig. 4c (main panel and inset). In blue we show the charge sensitivity as a function of tunnel rate for $S_{pp}(\omega) = S_{pp}(2\pi f_0)$ and $n^0_g = n^0_{g,\text{max}}$, which corresponds to the experimental situation presented earlier. For our experimental set-up and a range of tunnel rates, the fundamental limit of dissipative rf charge read-out is $\delta q \lesssim 70 \, \text{ne}\, \text{Hz}^{-\frac{1}{2}}$. As can be seen from the inset of Fig. 4c, the best charge sensitivity occurs for matching tunnel rate and excitation frequency. Adjusting $\Gamma_0$ and $f_0$ may thus be a route to obtain the best sensitivity, although experimental constraints such as the resonant circuit, that is, $f_0$, will set a practical limit.

We benchmark our detector’s ultimate sensitivity against that of rf-SETs predicted in ref. 47 (red trace in Fig. 4c). A direct comparison is made considering the tunnel resistance equivalent $R_t = 2k_B T / e \Gamma_0$, which sets the same tunnel rate at $\Delta E = 0$ for both cases. Comparing both curves, we find that rf-SETs exhibit a better fundamental charge sensitivity at high tunnel rates, whereas our rf gate sensor performs favourably at low $\Gamma_0$ that is, for highly resistive tunnel barriers, which is the usual scenario of quantum dots in the few-electron regime.

We confirm the accuracy of our simulations by comparing them to experimental data. In Fig. 4d we plot the ratio of power dissipated in the device, $\langle P \rangle$, and total dissipated power in the resonator, $P_0$, as a function of $V_g$ across a charge transition point. The lineshape of the peak presents a $\cos^2$ dependence (see equation 4) and is reproduced by our numerical simulations. Furthermore, we compare the experimental and theoretical dependence of $\langle P \rangle$ on tunnel rates. In the cyclical exchange of electrons between dot and electron reservoirs, $\langle P \rangle$ depends on the ratio of the drive frequency $\omega_0 = 2\pi f_0$ and the tunnel rate $\Gamma_0$, as seen in equation 4. While $\omega_0$ is fixed in the experiment, $\Gamma_0$ can be tuned by changing the profile of the tunnel barriers. This is controlled electrostatically by means of the back gate voltage $V_{bg}$. The effect of changing tunnel rates on the detector’s response is demonstrated in Fig. 4e, where we plot the maximum $\langle P \rangle / P_0$, arising from an exchange of electrons between QD1 and the drain reservoir (magenta arrow in Fig. 2c) as a function of $\Gamma_0$ (see Supplementary Fig. 3). The data are well fitted by our model (red line), and may be understood as follows. As low tunnel rates no additional power is dissipated in the device since there is insufficient time for electrons to tunnel at the rf-drive timescale (Fig. 4f). Equally, at high tunnel rates no power is dissipated as electron tunnelling is elastic (Fig. 4h). However, when $\Gamma_0 \approx 0.75 \omega_0$, power dissipation is maximized as on average tunnelling happens inelastically at the end of the rf cycle (Fig. 4g). The deviation from the expected $\Gamma_0 = \omega_0$ at which the dissipated power is maximized (see equation 4) could be a result of a small coupling asymmetry to the source and drain reservoirs of QD1 (see Supplementary Note 4).

**Dispersive readout.** We now move on to the analysis of dispersive readout and the limits of gate-based phase sensing. Here the change in the probability of the electron being in the dot because of the rf-drive generates a tunneling capacitance term given by,

$$C_s(t) = \frac{e}{V_g} \frac{dp_1}{dn^0_g} = \frac{e}{V_g \sqrt{\cos(\omega_0 f)}} \frac{dP_1(t)}{dn^0_g}$$

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which in turn generates a phase shift \( \Delta \phi(t) = -C(t) \). We confirm our calculations in Fig. 5a by comparing experimental data to the theoretical average phase shift \( \langle \Delta \phi \rangle \). Similarly to the average power dissipation, the phase response peaks at the degeneracy point and the change \( d\langle \phi \rangle / dn_0^0 \) is maximum close to \( n_0^{\text{max}} \). \( C_1 \) is always positive independently of \( T \) and \( \Gamma_0 \) and hence \( \langle \Delta \phi \rangle \) remains negative, which indicates that on average electron tunnelling leads the rf excitation unless the transient behaviour of the system is probed (see Supplementary Note 2). An analytical solution of equation (6) for \( \delta n_0 < k_B T / E_C \) confirms this result,

\[
\langle \Delta \phi \rangle \approx -\frac{\pi Q(e^2)^2}{C_p} \frac{1}{2k_B T \cosh^2 \left( \frac{\Delta \phi(0)}{2k_B T} \right)} \frac{1}{1 + \omega_0^2 / \Gamma_0^2} \tag{7}
\]

In contrast to the average power dissipation, \( \langle \Delta \phi \rangle \) does not peak at the resonant frequency and tends to a constant value for large \( \Gamma_0 \). This offers a way to maximize the dispersive signal while reducing the excess power dissipation.

The phase noise spectral density associated with the phase fluctuations is presented in Fig. 5b. It is maximum at multiple of \( 2f_0 \) with odd harmonics predominantly contributing to the noise spectrum. This can be explained from the time symmetry of the tunnelling capacitance: \( C_1 \approx \tan(\omega_0 t) \) is an odd function of time and periodic in \( 1/2f_0 \) (see Supplementary Note 3). Signal and noise are hence decoupled in frequency space offering an opportunity for high-sensitivity phase detection.

The detector’s ultimate phase sensitivity, \( \delta \phi \), is calculated in the same way as its charge counterpart (see equation (5)) as the ratio of phase noise \( \sqrt{\frac{S_{\phi \phi}}{n_0}} \) and change in average phase \( d\langle \phi \rangle / dn_0^0 \). It is plotted in Fig. 5c as a function of reduced tunnel rate at bias \( n_0^{\text{max}} \) and frequency \( \omega = 2\pi f_0 \). In tune with \( \phi \) the phase sensitivity has no minimum at \( f_0 \) but approaches a low constant value at high tunnel rate. For parameters corresponding
to our set-up the fundamental limit of phase sensitivity is \( \delta \theta \leq 0.04 \mu \text{rad Hz}\(^{-1/2}\) for tunnel rates \( \Gamma_{\text{e}} > \Gamma_{\text{f}} \). Fast gate-based phase detection is thus suitable for systems with transparent tunnel barriers, but performs also well at moderate tunnel rates. This result compares favourably to phase detection based on cooper-pair transistors, which provides sensitivities of the order of 1 \mu \text{rad Hz}\(^{-1/2}\) (ref. 50).

**Discussion**

In conclusion, we have reported the high-sensitivity resonant charge readout of a few-electron double quantum dot in silicon and studied its experimental and theoretical limits. The ultimate sensitivity of resonant readout, set by the Sisyphus noise arising in fast-driven two-level systems, is comparable to the best rf-SET charge sensors at an equivalent measurement bandwidth. Resonant gate-sensing can be introduced in all semiconductor materials where a strong coupling between gate and qubit can be engineered. A high sensitivity in situ readout can then be achieved by eliminating sources of excess dissipation such as losses in the inductor and substrate, providing a resonant circuit matching the high-gate impedance, and matching rf-excitation frequency to the electron tunnel rates. Resonant gate-sensing therefore offers a competitive alternative to external charge detectors. The combination of high sensitivity and large bandwidth will allow for single-shot readout of electron spins in semiconductors. Moreover, the flexibility of this technique, which eliminates the need for external sensor elements, opens up a window for high-fidelity, high-integration qubit architectures.

**Methods**

**Device fabrication.** The nanowire transistors used in this study were fabricated on SOI substrates with a 145-nm buried oxide. The silicon layer is patterned to create the nanowires by means of optical lithography, followed by a resist trimming process. For the gate stack, 1.9-nm HfSiON capped by 5 nm TiN and 50 nm polycrystalline silicon were deposited, leading to a total equivalent oxide thickness of 1.3 nm. The Si thickness under the HfSiON/TiN gate is 11 nm. After gate etching, a SiN layer (thickness 10 nm) was deposited and etched to form a first spacer on the sidewalls of the gate. 18-nm-thick Si raised source and drain contacts were selectively grown before the source/drain extension implantation and activation annealing. Then a second spacer was formed and followed by source/drain implantations, activation spike anneal and salicidation (NiPSi).

**Measurement set-up.** Measurements were performed at the base temperature of a dilution refrigerator. Radiofrequency reflectometry was performed at 335 MHz by embedding the sample in a resonant LC circuit formed by a surface mount inductor (390 nH) and the device’s parasitic capacitance to ground (500 fF). At low temperature and room temperature amplification, the reflected signal was fed in a quadrature demodulator, yielding the signal’s quadrature and in-phase component from which magnitude \( \gamma \) and phase \( \phi \) are calculated.

**Numerical calculations.** \( P(t) \) and all subsequent derivatives such as \( P(t') \) or \( \Delta \phi(t') \) are finite time series in the numerical calculations. \( P(t') \) was obtained by solving equation (2) numerically for a range of parameters corresponding to experimental constraints, namely \( f_{\text{e}} = 335 \text{ MHz}, \ T_{\text{e}} = 15 \text{ mK}, \ E_{\text{C}} = 15 \text{ meV} \) and \( \delta_{\text{e}} = 0.03 \), at equal time steps in the interval \( t = [0.05, 5] \). The averages \( \langle P \rangle \) and \( \langle \Delta \phi \rangle \) are taken over one full period. Owing to the finite time series nature of all variables no autocorrelation is necessary, but \( S_{\phi}(\omega) \) can be calculated immediately from the power (phase) fluctuations: \( S_{\phi}(\omega) = (\Omega^{2}/(b^{2}a^{2}d^{2}XN|\Delta|^{2})) \times e^{-\omega^{2}/2\omega_{\text{Q}}^{2}} \).

**References**

1. Collins, J. L. et al. Dispersive readout of a few-electron double quantum dot with fast rf gate sensors. Phys. Rev. Lett. 110, 046805 (2013).

2. van Wees, B. J. et al. Quantized conductance of point contacts in a two-dimensional electron gas. Phys. Rev. Lett. 60, 848–850 (1988).

3. Reilly, D. J., Marcus, C. M., Hanson, M. P. & Gossard, A. C. Fast single-charge sensing with a rf quantum point contact. App. Phys. Lett. 91, 162101 (2007).

4. Finley, M. C. et al. Single charge detection using a radio-frequency quantum point contact. App. Phys. Lett. 91, 222104 (2007).

5. Kastner, M. A. The single-electron transistor. Rev. Mod. Phys. 64, 849–885 (1992).

6. Schoelkopf, R. J., Wahlgren, P., Kozhevnikov, A. A., Delsing, P. & Prober, D. E. The radio-frequency single-electron transistor (rf-set): a fast and ultra-sensitive electrometer. Science 280, 1238–1242 (1998).

7. Liu, W., Li, Z., Pfeiffer, L., West, K. W. &结尾的引用，例如文献 [9] 提到的噪声源……
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Author contributions

A.C.B. and M.F.G.-Z. contributed equally to this work. A.C.B. and M.F.G.-Z. devised and performed the experiments; S.B. fabricated the sample; A.C.B. performed the calculations; M.F.G.-Z. and A.C.B. co-wrote the paper; A.J.F. contributed to the paper. A.J.F. acknowledges funding from EPSRC under the grant EP/K027018/1.

Additional information

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