Probing the effect of intragranular premature $\kappa$-carbide on incipient plasticity behavior in austenite-based Fe-Mn-Al-(Cr)-C steels

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ABSTRACT
The effect of nanoscale intragranular premature $\kappa$-carbide precipitates, having an ordered structure but without chemical partitioning, on the incipient plasticity behavior of austenite in Fe-Mn-Al-(Cr)-C low-density steels was investigated by nanoindentation. We found that the incipient plasticity was dominated by a heterogeneous dislocation nucleation mechanism via atom-vacancy exchange. Although the content of $\kappa$-carbide decreased with Cr addition, its negligible effect on incipient plasticity strength was witnessed by the slightly increased shear stress for dislocation nucleation. Comparatively, the increased interstitial C atoms with Cr content in austenite enhanced lattice cohesions which impeded the nucleation events by increasing the requisite shear stress.

IMPACT STATEMENT
Despite being one of the most important strengthening phases, nanoscale premature $\kappa$-carbide precipitates surprisingly have a negligible effect on incipient plasticity of austenite in Fe-Mn-Al-(Cr)-C low-density steels.

1. Introduction
Nanoscale $\kappa$-carbide is considered to be one of the most important strengthening phases in Fe-Mn-Al-C low-density steels [1–3]. For example, it has been shown to enhance yield strength in austenite-based steels by 340–480 MPa [2,3]. This enhancement was attributed to an ordering induced strengthening [3] whereby matrix dislocation sheared an ordered $\kappa$-carbide precipitate to create an antiphase boundary on the slip plane of the precipitate [4]. $\kappa$-carbide precipitation was also considered critical for planar dislocation glide during plastic deformation in austenite [2,5]. Indeed, incipient plastic deformation, i.e. the onset of permanent deformation, can be induced by the dislocation nucleation during elastic-plastic transformation [6–11]. It was suggested that the transition from atomistic deformation to continuum-level plasticity may be closely associated with dislocation nucleation [6]. However, no reports on incipient plasticity behavior were available till now, limiting one’s understanding on the role of $\kappa$-carbide on plasticity.

Instrumented nanoindentation has been found to be a powerful tool to assess incipient plasticity associated with different dislocation nucleation mechanisms in metallic materials [9–14]. The first pop-in event or split-off point
deviated from theoretical elastic deformation in a load-displacement ($P-h$) curve during indentation loading, are generally considered to be the response to dislocation nucleation at the incipient plasticity stage \cite{8,10,14}. It was found in a dual-phase Fe-Mn-C-Si steel that dislocations nucleating earlier in large ferrite grains than in small ferrite and austenite grains, were responsible for incipient plasticity \cite{14}. Nanoindentation tests also indicated a homogeneous dislocation nucleation mechanism in austenite grains of Fe-21Mn-11Al-1.5C-2Si (wt. %) steel spanning a range of processing conditions from solution, aging to thermo-mechanical treatments \cite{12}.

Our recent work \cite{15} has highlighted a new intragranular premature $\kappa$-carbide (2–3 nm in particle size) in Fe-20Mn-9Al-3Cr-1.2C (wt. %) low-density steel. As compared with the well-known coarsened $\kappa$-carbide \cite{3,16}, it has an ordered L1$_2$ structure but without detectable chemical partitioning with austenite at near-atomic scale. This means that the ordered L1$_2$ structure of the intragranular $\kappa$-carbide could be approximated as an FCC structure with an interstitial C atom occupying the body-centered octahedral position. Regarding the effect of interstitial atoms on incipient plasticity, it was suggested that dissolving 0.5 at. % C and 1.0 at. % N into a FeMnCoCr high entropy alloy (HEA) increased the activation volume and maximum shear stress necessary for the homogeneous dislocation nucleation to be triggered by a thermally activated displacement of a single principal atom \cite{10}. However, Y.X. Ye et al. \cite{9} proposed a heterogeneous dislocation nucleation mechanism via cooperative migration of multiple atoms in a NbTiZrHf HEA, where the interstitial O and N atoms induced an increase of critical shear stress but with no significant effect on activation process. Thus, in this work, we aimed to probe the effect of such an intragranular premature $\kappa$-carbide on incipient plasticity in austenite-based FeMn-Al-(Cr)-C steels using nanoindentation. Because of the suppression effect of the Cr alloying element on precipitation of $\kappa$-carbide \cite{17–19}, it was intentionally added in order to have representative sample states with and without $\kappa$-carbide.

2. Materials and methods

Four Fe-20Mn-9Al-(0, 3, 6 and 9) Cr-1.2C (wt. %) low-density steel samples, hereafter referred to as 0Cr, 3Cr, 6Cr and 9Cr, were studied. As detailed in our previous works \cite{20,21}, they were prepared by induction melting and centrifugal casting in an argon atmosphere with cooling rates in excess of $10^3$ K/s (namely near-rapid solidification). Scanning electron microscopy (SEM) characterization was carried out using a JEOL JSM-7800F microscope equipped with an electron backscatter diffraction (EBSD) detector and dedicated Channel 5 software was used for post- data treatment. Transmission electron microscopy (TEM) characterization was done using a FEI Tecnai G2-20 twin microscope, operated at 200 kV and a Thermo Fisher Titan Themis 60-300 microscope, operated at 300 kV. The latter was equipped with a probe aberration corrector for acquiring (high-resolution) scanning TEM ((HR)TEM) high-angle annular dark-field (HAADF) images. TEM specimens were prepared by twin-jet electrolytic polishing. Atomic probe tomography (APT) was performed using a local electrode atom probe instrument (CAMECA LEAP 4000 XHR), in laser-pulsed mode with a repetition rate of 200 kHz, a pulse fraction of 15%, and a specimen temperature of 50 K. APT specimen was prepared by standard two-step electro-polishing. A peak decomposition algorithm in IVAS 3.6.8 software was used to resolve peak overlapping among Fe, Al and Cr at 27 Da in mass spectrum for improving counting statistics \cite{22}. Quantitative chemical composition was also examined by an electron probe micro-analysis (EPMA)-8050G instrument, operated at 15 kV.

Mechanical properties of austenite were measured by an MTS XP nanoindenter, equipped with a Berkovich tip with a constant loading rate of 0.05 s$^{-1}$. One hundred indentations separated by 10 $\mu$m were tested, addressing thus the influence of different austenite grain orientations. The data of indentation completely realized within austenite matrix was used for further analysis. Bader charge transfer was calculated using density functional theory (DFT) implemented in a Vienna ab initio simulation package (VASP). More description of the nanoindentation experiments and calculation can be found in the Supplementary Information.

3. Results and discussion

As shown in Figure 1(a-d), the volume fractions of the island-like ferrite phase in the 0Cr, 3Cr, 6Cr and 9Cr samples were respectively, 3%, 8%, 17% and 27%. Figure 1(e-g) indicate that the nanoscale intragranular $\kappa$-carbides are present in the austenite matrix of all the 0Cr, 3Cr and 6Cr samples and their average sizes were estimated as $\sim$ 5 nm, $\sim$ 3 nm and $\sim$ 1 nm, respectively. The classical cube-on-cube orientation relationship between $\kappa$-carbides and $\gamma$-austenite of $[100]_\kappa$ // $[100]_\gamma$ and $(001)_\kappa$ // $(001)_\gamma$ \cite{1} is confirmed by selected-area electron diffraction (SAED) patterns (insets in Figure 1(e-g)). No superlattice reflection indicates that the existence of intragranular $\kappa$-carbides is invisible in the 9Cr sample (Figure 1(h)). Thus, the increase of Cr content leads to an increase in the ferrite content and a suppression of intragranular $\kappa$-carbide precipitation in austenite.
Consistent with our results from the 3Cr sample [15], the structure and chemistry of nanoscale intragranular \( \kappa \)-carbide are better revealed by HRSTEM-HAADF and APT, respectively. For example, the ordered \( \kappa \)-carbide domains in the austenite matrix of the 0Cr sample, marked by red circles in Figure 2 (a), are clearly identified using FFT patterns. According to the simulated STEM-HAADF images in Figure 2(b), these \( \kappa \)-carbides have an ordered \( \text{L}'1_2 \) structure, assuming the non-stoichiometric C atom is located at the body-center octahedral site of the FCC structure. The APT result in Figure 2(c) shows the uniform distributions of all the Fe, Mn, Al and C constituent elements. The corresponding \( \mu \) values (Figure 2(d)) of all the elements are close to 0, further indicating that they are randomly distributed on a near-atomic scale in the austenite [23,24]. It is confirmed here that the near-rapid solidification process resulted in the formation of intragranular premature \( \kappa \)-carbides in all the 0Cr, 3Cr [15] and 6Cr (result not given) samples.

Figure 3 shows that no significant pop-in events are observed in any of the samples tested by nanoindentation (the partial enlarged figures are shown in Figure S2 of Supplementary Information), suggesting a smooth and continuous deformation behavior. This could be caused by the high solid solution C content, which reduces the mean free path of mobile Shockley partial dislocations hence limiting plastic flow during deformation [10]. Providing that initial elastic deformation of the indented material follows the relation obtained by the Hertzian contact mechanics model [25], the deviation of the measured \( P-h \) curve from the Hertzian curve can be defined as the onset of plasticity [10,14,26,27]. Based on this model, the elastic response from a specimen surface layer is expressed by:

\[
P = \frac{4}{3} \frac{E_r}{R_i} \frac{1}{h^2}
\]

where \( P \) is the applied load, \( R_i \) is the tip radius of the indenter (\( \sim 200 \) nm, identified by fitting the initial elastic portion of the \( P-h \) curves with the Hertzian contact law [28]), \( h \) is the displacement of indent and \( E_r \) is the reduced modulus given by:

\[
\frac{1}{E_r} = \frac{1 - \nu_i^2}{E_i} + \frac{1 - \nu_s^2}{E_s}
\]

where \( E \) and \( \nu \) are the Young’s modulus and Poisson’s ratio, respectively. The subscripts \( i \) and \( s \) represent the indenter and sample, respectively. In this work, \( E_i, \nu_i \) and \( E_s, \nu_s \) are 1141 GPa [27], 0.07 [27] and 0.33 [29], respectively, and the \( E_r \) of different samples are shown in Table 1.

To quantitatively analyze the elastic-plastic deformation of austenite with and without \( \kappa \)-carbide, the maximum shear stress (\( \tau_{max} \)) beneath the indenter required

\begin{table}
\centering
\begin{tabular}{|c|c|c|c|c|}
\hline
Samples & \( E \) (GPa) & \( E_r \) (GPa) & Range of \( \tau_{max} \) (GPa) & \( \bar{\tau}_{max} \) (GPa) \\
\hline
0Cr & 191.94 ± 2.33 & 181.33 ± 1.85 & 6.67–7.36 & 7.06 ± 0.20 \\
3Cr & 188.55 ± 2.80 & 178.62 ± 2.24 & 6.71–7.50 & 7.09 ± 0.25 \\
6Cr & 194.79 ± 2.72 & 183.34 ± 2.15 & 6.81–7.54 & 7.18 ± 0.22 \\
9Cr & 192.29 ± 2.55 & 181.61 ± 2.02 & 6.86–7.80 & 7.18 ± 0.26 \\
\hline
\end{tabular}
\caption{The measured Young’s modulus \( E \), reduced modulus \( E_r \), range of \( \tau_{max} \) and average \( \bar{\tau}_{max} \) of the studied samples.}
\end{table}
to trigger incipient plasticity can be calculated from [25]:

$$\tau_{\text{max}} = \frac{0.31}{\pi} \left( \frac{6PE^2}{R_i^2} \right)^{\frac{1}{2}}$$

where $P$ is the load at which incipient plasticity occurs. The $\tau_{\text{max}}$ values (Table 1), can be determined from the $P-h$ curves of each sample. It is clear that $\tau_{\text{max}}$ slightly increases with Cr content (the range of calculated $\tau_{\text{max}}$ values is shown in Figure S3 of Supplementary Information). Since the nanoscale intragranular $\kappa$-carbides are uniformly distributed in austenite (see Figures 1 and 2) and the radius of the indenter tip is much larger than the distance between $\kappa$-carbides, the incipient plasticity strength is thus the reliable response to the overall mechanical properties of austenite. The fact that the volume fraction of intragranular premature $\kappa$-carbides decreases with increasing Cr content (Figure 1) indicates that other factor than the presence of intragranular premature $\kappa$-carbides is dominating the $\tau_{\text{max}}$, as will be discussed below.

In addition, cumulative probability $f$ correlated with $\tau_{\text{max}}$ on the onset of incipient plasticity, is used to investigate the activation volume ($\Omega_r$) for dislocation nucleation by Schuh’s model [6,28]:

$$\ln[-\ln(1-f)] = \frac{\Omega_r}{kT} \tau + \beta$$

where $k$ is the Boltzmann constant, $T$ is the temperature and $\beta$ is a weak function of shear stress. According to Equation (4), the slope $\frac{\Omega_r}{kT}$ can be determined by plotting and fitting $\ln[-\ln(1-f)]$ vs. $\tau$. Accordingly, the $\Omega_r$ of each sample can be deduced, as shown in Figure 3(b).
An atomic volume $\Omega$ is $0.25a_0^3$ [10] where the lattice constant $a_0$ of $\sim 3.7$ Å in austenite of the samples was measured by X-ray diffraction (XRD), as detailed in the Supplementary Information. Thus, the $\Omega$ of austenite is calculated as 12.66 Å$^3$, and the calculated $\Omega_v$ for dislocation nucleation in the 0Cr, 3Cr, 6Cr and 9Cr samples are 25.26 Å$^3$ (2.00 $\Omega_v$), 20.89 Å$^3$ (1.65 $\Omega_v$), 17.44 Å$^3$ (1.38 $\Omega_v$) and 14.31 Å$^3$ (1.13 $\Omega_v$), respectively.

As shown in Table 1, the measured $\tau_{\text{max}}$ is close to the theoretical shear strength ($\sim 1/10 \mu$, the shear modulus $G$ of austenite is 70 GPa [5]). According to the relationship $M = \frac{\tau_0}{\sigma_y}$ [30], where $M$ is the Taylor factor (3.06 [5]), $\sigma_y$ is the yield strength (the $\sigma_y$ of 0Cr sample is 836 MPa [17]) and $\tau_0$ is the critical resolved shear stress for dislocation slip, $\tau_0$ is calculated as $\sim 273$ MPa. This value is much smaller than the measured $\tau_{\text{max}}$. Thus, it can be considered that the incipient plasticity is controlled by dislocation nucleation [9–11,31], rather than the slip of pre-existing mobile dislocations. The obtained $\Omega_v$ values are in the range of 1–2 $\Omega$, in between the $\Omega_v$ of $\sim 1 \Omega$ for homogeneous nucleation and the several atomic volumes (2–5 $\Omega_v$) required for heterogeneous nucleation via vacancy clusters or multiple-atom cooperative migration [8,10,11]. This suggests that the dislocation nucleation mechanism in all the investigated samples is heterogeneous nucleation via conventional atom-vacancy exchange [8,11].

Based on the results above, the intragranular premature $\kappa$-carbide has a negligible effect on the incipient plasticity, a phenomenon was also observed in Mo-added austenitic steels by J. Lee et al. [32]. Since the proposed heterogeneous dislocation nucleation is a stress-assisted thermally activated process [9,10,28], the effects of vacancy concentration and lattice inherent cohesion

**Figure 3.** (a) Typical load-displacement $(P-h)$ curves of austenite in the 0Cr, 3Cr, 6Cr and 9Cr samples; (b) corresponding relationship between $\ln[-\ln(1-f)]$ and $\tau_{\text{max}}$ for deducing the activation volume through linear fitting.
Table 2. Quantitative compositions of austenite in the 0Cr, 3Cr, 6Cr and 9Cr samples (at. %) determined by EPMA.

| Samples | Fe     | Mn     | Al     | C      | Cr     |
|---------|--------|--------|--------|--------|--------|
| 0Cr     | 60.45 ± 0.95 | 18.97 ± 0.33 | 15.00 ± 0.21 | 5.58 ± 0.33 | –      |
| 3Cr     | 57.01 ± 0.91 | 19.04 ± 0.76 | 15.11 ± 0.06 | 5.83 ± 0.21 | 3.01 ± 0.14 |
| 6Cr     | 53.94 ± 0.83 | 19.34 ± 0.65 | 15.22 ± 0.15 | 6.12 ± 0.30 | 5.36 ± 0.40 |
| 9Cr     | 51.08 ± 0.49 | 19.92 ± 0.47 | 15.38 ± 0.12 | 6.30 ± 0.31 | 7.32 ± 0.15 |

Figure 4. Proposed atomic structural models of the FCC structure used to calculate bader charge transfer between interstitial C atom and metallic atoms in the first neighboring coordination shell: (a) and (b) are the models with a C atom occupying a central octahedral site, while (b) has a Fe atom substituted by a Cr atom; (c) and (d) are the models with a C atom occupying a tetrahedral site, while (d) has a Fe atom substituted by a Cr atom.

must also be considered [9,10]. On the one hand, the same near-rapid solidification process resulted in nearly the same vacancy concentration in all four analyzed samples, which indicates a negligible effect of vacancy concentration variation. On the other hand, the solid-solution composition evaluation in austenite with Cr addition is an important factor affecting lattice inherent cohesion. Table 2 indicates that the Mn, Al and C elements contents in austenite all increase with Cr content. Metallurgically, the minor change of Mn and Al should have a limited impact on mechanical properties. However, the interstitial solutes generally have a huge impact on the incipient plasticity of different materials [9,10,33]. For example, interstitial solutes N/O have been found to induce local charge transfer enhancing lattice cohesion, which in turn increases the critical shear stress required for the onset of plasticity in NbTiZrHf HEA [9].

To further elucidate the lattice cohesion change caused by the increased C and Cr contents, the local charge transfer between interstitial C atom and surrounding
metallic atoms in FCC structure was calculated. The bader charge reflects the number of electrons localized near a particular atomic core [9], which is generally used as an effective tool to analyze the charge transfer among atoms. In this work, the interstitial C atoms are situated in octahedral and tetrahedral sites of the FCC structure as shown in Figure 4. Due to no detectable chemistry difference between the premature κ-carbide and austenite matrix (Figure 2), the structures where the C atoms are located in the octahedral site (Figure 4(a) and (b)) correspond to the premature κ-carbide. In addition, the Cr content change is considered by changing the number of nearest neighbor Cr atoms to C atom. It should be noted that the charge numbers on the outer layers of the ground states Fe, Mn, Al, Cr and C atoms are 8, 7, 3, 6 and 4, respectively. It is found that regardless of whether the interstitial C atom is in an octahedral or tetrahedral site, it always attracts significant electrons from its surroundings, decreasing thus the bader charges of the surrounding metallic atoms, as shown in Figure 4. However, the addition of Cr atoms has little effect on charge transfer. Note that the charge transfer between interstitial C atom and nearby metallic atoms is anticipated to transform the original metal–metal bond to ionic-like metal–carbon bonds, which results in enhanced atomic cohesion [9]. Thus, the calculated charge transfer suggests that the increased concentration of interstitial C atoms in austenite with Cr content (Table 2) significantly increases overall atomic cohesion, which in turn impedes dislocation nucleation events by increasing τmax for incipient plasticity (Table 1).

4. Conclusion

In summary, we found that the incipient plasticity of all the studied samples (with and without intragranular premature κ-carbide) was dominated by a heterogeneous dislocation nucleation mechanism via atom-vacancy exchange. The decreased intragranular premature κ-carbide content and the concurrent slight increase of the maximum shear stress indicated the negligible effect of intragranular premature κ-carbide on incipient plasticity. However, the interstitial C content in austenite played a key role in dislocation nucleation. This was because the interstitial C atoms, as we show, induced local charge transfer leading to enhanced lattice cohesion, which in turn increased the shear stress for dislocation nucleation events.

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Disclosure statement

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