Unveiling Sub-pc Supermassive Black Hole Binary Candidates in Active Galactic Nuclei

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Abstract

The elusive supermassive black hole binaries (SMBHBs) are thought to be the penultimate stage of galaxy mergers, preceding a final coalescence phase. SMBHBs are sources of continuous gravitational waves, possibly detectable by pulsar timing arrays; the identification of candidates could help in performing targeted gravitational wave searches. Due to SMBHBs’ origin in the innermost parts of active galactic nuclei (AGN), X-rays are a promising tool for unveiling their presence, by means of either double Fe Kα emission lines or periodicity in their light curve. Here we report on a new method for selecting SMBHBs by means of the presence of a periodic signal in their Swift Burst Alert Telescope (BAT) 105 month light curves. Our technique is based on Fisher’s exact t-test and takes into account the possible presence of colored noise. Among the 553 AGN selected for our investigation, only the Seyfert 1.5 galaxy Mrk 915 emerges as a candidate SMBHB; from subsequent analysis of its light curve we find a period $P_0 = 35 \pm 2$ months, and the null hypothesis is rejected at the $3.7\sigma$ confidence level. We also present a detailed analysis of the BAT light curve of the only previously X-ray-selected binary candidate source in the literature, the Seyfert 2 galaxy MCG+11-11-032. We find $P_0 = 26.3 \pm 0.6$ months, consistent with the one inferred from previously reported double Fe Kα emission lines.

Unified Astronomy Thesaurus concepts: X-ray active galactic nuclei (2035); Seyfert galaxies (1447)

1. Introduction

It is now well established that massive galaxies host supermassive black holes (SMBHs, $M_{BH} \gtrsim 10^6 M_\odot$) in their central regions (e.g., Kormendy & Ho 2013). Such extreme astrophysical objects are likely linked to the evolution of their host galaxies. In fact, stellar bulge properties, such as velocity dispersion (e.g., Ferrarese & Merritt 2000) and stellar mass (e.g., Häring & Rix 2004), are found to correlate with the mass of the central SMBH.

In a cold dark matter ($\Lambda$CDM) cosmological models galaxies grow hierarchically through frequent mergers (e.g., Cole et al. 2000; Volonteri et al. 2003). Galaxy mergers have been proposed as one of the main mechanisms by which nuclear activity, star formation and outflows are triggered (e.g., Di Matteo et al. 2005; Hopkins et al. 2006; Di Matteo et al. 2008). One of the most interesting possible outcomes of this process is the formation of an SMBH binary (SMBHB) system. During a galaxy merger, if both SMBHs are accreting at kiloparsec-scale distance from each other, the source will appear as a dual active galactic nucleus (AGN; e.g., Koss et al. 2012; McGurk et al. 2015; De Rosa et al. 2018, 2019; Koss et al. 2018, and references therein). Subsequently, the two SMBHs drift toward the center of mass because of dynamical friction (Dosopoulou & Antonini 2017) and form an inspiraling binary system at subparsec-scale separations (e.g., Begelman et al. 1980), which will eventually merge (e.g., Dotti et al. 2012; Mayer 2013; Colpi 2014). Theoretical models predict that, after the two black holes bind in a binary, dynamical friction becomes inefficient, possibly preventing the binary from merging in a time shorter than the Hubble time (e.g., Milosavljević & Merritt 2003). However, in the presence of nuclear gas inflows (e.g., Dotti et al. 2012), or deviations from spherical symmetry in the potential of the nucleus (Sesana & Khan 2015), the binary can still transfer enough energy to its surroundings to merge within $t_{\text{cool}} \sim 1$ Gyr. Despite the expected abundance of such objects, the detection of SMBHBs remains elusive and only limited indirect observational evidence has been found so far (see De Rosa et al. 2019 for a recent review). This is mainly due to the angular resolution of current telescopes, which do not have a resolving power below a few parsecs at most redshifts and wavelengths (e.g., Rodriguez et al. 2006), insufficient to distinguish emitting binary systems.

Hydrodynamic numerical simulations usually assume that an SMBHB excavates a cavity in the surrounding gas, which forms a circumbinary accretion disk (e.g., Noble et al. 2012;
Farris et al. 2015). At smaller scales, accretion possibly occurs through minidisks around each black hole inside the cavity (e.g., Hayasaki et al. 2008; D’Ascoli et al. 2018). While the circumbinary disk is thought to be responsible for the optical and IR emission (D’Orazio et al. 2015), the UV and X-rays should be mainly emitted by the inner minidisks (Sesana et al. 2012; D’Ascoli et al. 2018). In particular, the UV and X-ray fluxes are expected to be periodic, since the accretion rate of the minidisks is periodically fed by streams of gas flowing from the outer circumbinary disk (e.g., Hayasaki et al. 2008; Haiman et al. 2009; Farris et al. 2015), with periods comparable to the binary period. Assuming a Keplerian regime, for SMBHBs with a separation of the order of \(10^{-5}\) pc, we expect a periodicity with periods longer than about a year. As these emissions originate very close to each black hole, UV and X-ray periodic modulation (e.g., Sesana et al. 2012; Roedig et al. 2014; Farris et al. 2015; Haiman 2017) can be used to identify possible SMBHBs. Additionally, the two minidisks may produce double-peak Fe Kα emission lines in the X-ray band (e.g., Popović 2012; Sesana et al. 2012; McKernan & Ford 2015), with energies Doppler-shifted by the minidisk relative to orbital motion. So far, the only X-ray-selected SMBHB candidate is the Seyfert 2 galaxy MCG+11-11-032 (Severgnini et al. 2018). The detection of two peaks (at \(4\sigma\) and \(2\sigma\), respectively) in the Fe Kα energy range, along with the visually identified harmonic behavior of the 123 month Swift Burst Alert Telescope (BAT) X-ray light curve with a period of \(P \sim 25\) months, strongly suggests the presence of an SMBHB.

Periodical variability from the inflow streams is also expected in the optical band, although it may be overwhelmed by the non-periodic emission from the circumbinary disk. Despite the fact that the UV and X-ray data are likely the best electromagnetic (EM) bands for periodicity searches in AGN, regular monitoring observations in these bands, spanning several years, are rare. For these reasons, the search for EM periodicity has been mainly undertaken in the optical band. Graham et al. (2015a) found 111 optically selected SMBHB candidates in the Catalina Real-Time Survey (Drake et al. 2009), and Charisi et al. (2016) identified 33 further objects in the Palomar Transient Factory (Rau et al. 2009). In addition, the presence of a periodic signal has been reported in single-source studies, such as of OJ 287 (e.g., Sillanpaa et al. 1988), PG 1302-102 (Graham et al. 2015b), NGC 5548 (Bon et al. 2016; Li et al. 2016), and more recently Mrk 231 (Kovačević et al. 2020). In particular, OJ 287 shows recurring flares with a precision so high that it is possible to predict the following flare with an accuracy of \(~4\) hr on a ~12 yr period (Laine et al. 2020). However, a significant fraction of those candidates are likely false positives. In fact, such a large number of SMBHBs should have produced a gravitational wave (GW) cosmic background above the current pulsar timing array (PTA) limit (see Arzoumanian et al. 2018 for the latest NANOGrav Collaboration limit, Lentati et al. 2015 for the latest European PTA limit, and Shannon et al. 2015 for the Parkes PTA limit), while no detection has been reported so far (Sesana et al. 2018).

By exploiting the 105 Month Swift-BAT Survey (Oh et al. 2018), here we propose a novel method to search for periodicities in colored noise X-ray light curves based on Fisher’s exact g-test (Fisher 1929) and its probability of false alarm due to colored noise fluctuations. A recent analysis of the X-ray light curves of a subsample of \(~220\) AGN, selected by their large excess variance, of the BAT survey (Liu et al. 2020) did not find any AGN with evidence for periodic behavior in their X-ray light curves. The search was based on the power spectrum fitting (Vaughan 2005) of colored noise light curves, i.e., those curves whose power spectral densities are not flat, or white (see Section 3 for details).

The paper is structured as follows: in Section 2 we review the power spectrum and the X-ray variability tools usually adopted, while in Section 3 we describe the proposed search method on simulated light curves. In Section 4 we apply the method to real X-ray light curves in the 105 Month Swift-BAT Survey and test the selected candidates by using sinusoidal fitting and epoch folding techniques. MCG+11-11-032 is also discussed in Section 5. Finally, we summarize and discuss our results in Section 6.

Throughout the paper, we adopt a flat ΛCDM cosmology with an accuracy of \(\sigma_\Lambda = 0.7\) and \(\sigma_M = 0.3\).

2. Identifying a Periodic Trend in a Stochastic Light Curve

X-ray emission from AGN is well known to be very variable (e.g., Markowitz & Edelson 2004; McHardy et al. 2004; Vagnetti et al. 2016; Falocco et al. 2017), even at hard energies (\(E > 10\) keV; e.g., Soldi et al. 2014). The X-ray variability of AGN is typically a superposition of stochastic processes and therefore is not easily modeled as a function of time and is usually referred to as noise.

Identifying periodic trends in light curves may result in a challenging task, because a sinusoidal or quasi-sinusoidal curve may be hidden in noise and be hardly recognizable in the time domain. A very powerful tool for identifying periodicities is the power spectral density (PSD), or power spectrum, which represents the mean value of the squared amplitude as a function of the temporal frequency \(f\). The most frequently used tool to represent the power spectrum is the periodogram \(P(f)\), which is defined as the squared Fourier transform of the light curve, i.e., \(P(f) = \left| \hat{X}(f) \right|^2 = \hat{X}(f) \times \hat{X}^*(f)\), where \(\hat{X}\) is the Fourier transform of the light curve \(x(t)\) and \(\hat{X}^*\) its complex conjugate.\(^ {17}\) We subtract the mean value of the light curve \(x_0 \equiv \langle x(t) \rangle\) before computing the Fourier transform, to remove the constant component of the light curve. We also neglect all frequency values larger than or equal to the Nyquist frequency \(f_{\text{Nyq}} = 1/2\delta t\), where \(\delta t\) is the sampling time, and their corresponding periodogram values, in order to exclude points due to aliasing. Several normalizations may be defined for the periodogram (e.g., Papadakis & Lawrence 1993; Vaughan et al. 2003; Emmanoulopoulos et al. 2016), but since we intend to study individual sources one by one (see Section 4), we choose a unitary normalization, and therefore \(P(f) = \left| \hat{X}(f) \right|^2\). This quantity is ideal for finding periodicities, given that the response to a pure sinusoid is a Dirac \(\delta\)-function. PSD is regularly used to identify periodicities in pulsar astronomy at many EM bands (e.g., Israel et al. 2016; Ambrosino et al. 2017; Mickaliger et al. 2018), to search for their continuous GW counterparts (e.g., Aasi et al. 2015), to detect quasi-periodic periodicities.

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\(^ {16}\) Excess variance (e.g., Nandra et al. 1997) is a parameter that quantifies variability, defined as \(\sigma^2_\text{ex} = S^2 - \sigma^2\), where \(S^2\) is the variance of the light curve and \(\sigma\) is the photometric error.

\(^ {17}\) It should be recalled that all real and simulated data are discrete, although to simplify the notations we will denote them as continuous throughout the whole article.
oscillations in X-ray binaries (e.g., Zhang et al. 1996), and to search for both short-term (e.g., Gierlinski et al. 2008; Miniutti et al. 2019) and long-term periodicities in AGN light curves (e.g., Bon et al. 2016; Liu et al. 2020). Moreover, the Fourier transform operator is linear, and if our light curve is given by

\[ x(t) = S(t) + N(t) \]

where \( S(t) \) is a sinusoidal component with temporal frequency \( f_0 \). If the light curve is sufficiently long, an analysis in the frequency domain will identify the periodicity, even if a sinusoidal signal with a small amplitude does not manifest in the light curve due to a low signal-to-noise ratio. This is evident in Figure 1, where we simulate a white noise-dominated time series, superposed to a signal with amplitude 10 times smaller than that of the noise. While inspection of the time series does not show any evidence for the presence of a periodicity, the power spectrum shows an evident peak at \( f_0 = 10^{-3} \) Hz, corresponding to the simulated sinusoid frequency.

2.1. Computing Significance above Underlying White Noise

Depending on the power of the periodic component with respect to the underlying noise, the peak in the periodogram will be more or less prominent. Typically, the greater the number of periods sampled in the light curve, the more prominent the periodic peak in the frequency domain, but quantifying its significance is not trivial. A common tool for estimating the significance of a peak above the underlying white noise is so-called Fisher’s exact g-test (Fisher 1929). If one wants to analyze a peak at the frequency \( f_0 \), the test consists in computing the value

\[ g_0 = \frac{P_S(f_0)}{N} \sum_{k=1}^{N} P_S(f_k) \]

where \( N \) is the number of points in our periodogram. The value \( g_0 \) corresponds to a p-value of

\[ p = P(g > g_0) = \sum_{k=1}^{b} (-1)^{k-1} \frac{N!}{k!(N-k)!} (1 - kg_0)^{N-k} \]

where \( b = \text{floor}(1/g_0) \), i.e., the largest integer smaller than \( 1/g_0 \). Given the presence of factorial calculations, Equation (1) is computationally impractical for very long light curves. We test whether our software is able to compute g-test p-values for light curves with up to \( \sim 5 \times 10^3 \) data points. Computing p-values of longer time series hence requires other tests to be used, but it is beyond the scope of this paper.

3. Simulations of Colored Noise Light Curves

The validity of the g-test is unfortunately limited to cases in which non-periodic noise is white. In fact, the power spectrum of the stochastic component of an AGN X-ray light curve is typically modeled as \( P_S(f) \propto f^\alpha \), in the absence of slope breaks in the sampled frequency range. In the case of white noise PSD, the slope \( \alpha \) will be approximately zero. However, it is well known that underlying noise in X-ray light curves of AGN is not white; typically, one finds colored noise distributions, with slope values of \( \alpha \sim -1.5 \) in the frequency range \( \log(f/\text{Hz}) \gtrsim -6 \) (e.g., Green et al. 1993; Lawrence & Papadakis 1993; Allevato et al. 2013; Emmanoulopoulos et al.)
of the Gaussian distribution is a typical value in the considered count rate range, while the standard deviation is the mean value of the photometric error. We verify that the results do not depend on the particular mean value we adopt in the range \(-3.3 \lesssim \log (CR/\text{cts s}^{-1}) \lesssim -1.5\), or on the average value of the photometric error.

For \(N\) sources with white noise light curves, the probability of finding one false periodicity by chance is given by \(p(\text{FA}|\alpha = 0) = 1/N\), which is \(p = 0.0018\) for \(N = 553\). Therefore, the \(g\)-test significance for white noise power spectra will be considered acceptable if the \(p\)-value satisfies \(p_{\text{val}} \leq p_{\text{th}} = 0.0018\). To check this procedure, we simulate \(10^6\) purely white noise light curves, i.e., without any injected periodicity, we perform \(g\)-tests on each and we flag every source with \(p_{\text{val}} \leq p_{\text{th}}\). The false alarm probability is given by the number of flagged light curves over the total number. As expected, we find \(p(\text{FA}|\alpha = 0) \approx 0.0018\). This is clearly not true for \(\alpha \neq 0\); therefore we need to simulate light curves for different values of \(\alpha\) and thus calculate \(p(\text{FA}|\alpha)\).

In order to simulate colored noise light curves, we adopt the technique presented by Kasdin (1995), which we summarize in the following. We simulate a white noise light curve \(x^{(w)}(t)\) as previously described, and its Fourier transform is \(\tilde{x}^{(w)}(f) \propto f^0\). It is possible to simulate a colored noise light curve, described by its spectral slope \(\alpha\), by defining the filter \(H(f) = f^{\alpha/2}\). We can introduce the quantity \(\tilde{x}^{(c)}(f) = \tilde{x}^{(w)}(f) \times \tilde{H}(f) \propto f^{\alpha/2}\), whose inverse Fourier transform is \(x^{(c)}(t)\). The periodogram of such a light curve is \(P_S(f) = |\tilde{x}^{(c)}(f)|^2 \propto f^{\alpha}\); therefore by construction the simulated light curve \(x^{(c)}(t)\) is made up of a stochastic colored noise process with spectral slope \(\alpha\).

These simulations can be used to quantify the expected number of false alarms in colored noise curves. We consider \(\alpha\) in \([-2, 1]\), spaced by \(\delta\alpha = 0.01\). For each value of \(\alpha\) we simulate \(10^5\) light curves following the above-described procedure. Again, for each value of \(\alpha\), we count the light curves with \(p_{\text{val}} \leq 0.0018\) and divide such number by \(10^5\), hence tracing \(p(\text{FA}|\alpha)\) in the selected interval, as shown in Figure 3.

4. Analysis of Real Swift-BAT Data

4.1. Identification of Periodic Candidates

A first step to identify candidates is to perform \(g\)-tests on the sample of 553 Swift-BAT sources presented above, using the following multi-step approach: (i) we do not make any assumption on the nature of the stochastic noise of the light curves, i.e., we assume that they are all characterized by white noise. (ii) We identify the highest PSD peak, and we test such a peak against the rest of the PSD, assumed as noise. We only consider peaks at periods \(9 \leq P_0 \leq 35\) months. The lower limit is set by the PTA sensitivity curve (e.g., Lentati et al. 2015), while the upper limit is set by the requirement that we observe at least three phases in a 105 month light curve, i.e., \(105/3 = 35\) months. (iii) We select all those sources whose \(p\)-values satisfy the condition \(p_{\text{val}} \leq 1/553 = 0.0018\), which is the threshold corresponding to the probability of finding one false positive by chance in the total sample analyzed, without setting any prior. (iv) Once the candidates are identified, we investigate whether they are dominated by colored noise fluctuations or not, and then estimate the probability that the periodic component is real.
Only two sources survive the first screening. The first one is the blazar Mrk 421, which has a PSD peak at $f_0 = 18 \pm 2$ nHz, corresponding to a period of $P_0 = 21 \pm 2$ months, with $P_{\text{val}} = 5 \times 10^{-4}$. The other selected AGN is the Seyfert 1.5 galaxy Mrk 915, with a PSD peak at $f_0 = 11 \pm 2$ nHz, corresponding to the period $P_0 = 35^{+5}_{-7}$ months, with $P_{\text{val}} = 8 \times 10^{-4}$, a factor of about 3.6 and 2.3 below the threshold $P_{\text{val}} = 0.0018$, respectively. We note that the uncertainties are given by the frequency resolution of the PSD at the peak frequency $f_0$.

The initial screening does not take into account the intrinsic color of the stochastic noise, i.e., the slope of the PSD. Assuming a simple power-law model with no breaks in the sampled frequency range for the PSD, i.e., $P_S(f) \propto f^\alpha$, the slope can be computed with linear fits between the logarithmic values of log $P_S$ and log $f$ (e.g., Papadakis & Lawrence 1993). We compute $\alpha$ for each source, with its normalized distribution shown in Figure 4. We note that the bulk of our sample has SSD slopes $-0.5 \leq \alpha \lesssim 0.5$, with a tail of very few sources characterized by $\alpha \lesssim -0.5$. Even though the typical slope at higher frequencies is $\alpha \sim -1.5$ (e.g., Allevato et al. 2013), this result is not surprising, since the X-ray PSD of AGN is expected to break to lower slopes at frequencies $f \lesssim 10^{-6}$ Hz (Shimizu & Mushotzky 2013), with PSD breaks observed in a few sources so far (Markowitz et al. 2003; McHardy et al. 2007; MacLeod et al. 2010). For this sample, a break timescale smaller than the Nyquist period, i.e., $T_{\text{br}} \lesssim 2$ months (or $f_{\text{br}} \gtrsim 2 \times 10^{-7}$ Hz), for 98% of the sources has been estimated by Liu et al. (2020), which means that the PSD break happens at much shorter timescales than those sampled by Swift-BAT, explaining the distribution of $\alpha$ shown in Figure 4.

The slopes of the PSDs for the two $g$-test selected candidates, Mrk 421 and Mrk 915, are $\alpha = -1.2 \pm 0.2$ and $\alpha = -0.4 \pm 0.3$, respectively. This means that Mrk 421 is one of those outliers that maintain red noise behavior even at extremely low frequencies, while Mrk 915 is characterized almost completely by white noise. We estimate the number of expected false alarms as the product of the false alarm probability for a given $\alpha$, $p(\text{FAP}(\alpha))$ (see Figure 3), and the probability of $\alpha$, $p(\alpha)$ (see Figure 4), multiplied by the number of sources $N = 553$, i.e., $N_{\text{exp}} = N p(\text{FAP}(\alpha)) p(\alpha)$. Concerning Mrk 915, for $\alpha = -0.4$ we re-simulate $p(\text{FAP}(\alpha = -0.4)$, using $P_{\text{val}} = 8 \times 10^{-4}$ as the threshold, obtaining $N_{\text{exp}} \approx 0.1$ expected false alarms. As for Mrk 421 ($\alpha = -1.2$, $P_{\text{val}} = 5 \times 10^{-4}$), we obtain $N_{\text{exp}} \approx 0.7$. This means that, assuming Poissonian distributions with expected value $N_{\text{exp}}$, the probability that Mrk 915 is a false positive is $\sim 6\%$, while for Mrk 421 such probability is $\sim 32\%$.

The high chance of Mrk 421 being a non-periodic component is supported by the fact that the source is well known to recurrringly flare in all bands (e.g., Aleksić et al. 2015), including the X-ray bands (e.g., Stroh & Falcone 2013; Hervet et al. 2019). As shown in Figure 5, the source has numerous flares of various intensities at $\sim 20$, $\sim 41$, $\sim 63$ and $\sim 83$ months from the beginning of the survey. It is therefore straightforward to conclude that the PSD indeed indicates a recurring variability pattern with a typical timescale of $P_0 \sim 21$ months, but it is clearly not due to a proper sinusoidal behavior of the light curve. Moreover, it is well known that, for blazars like Mrk 421, the dominant X-ray emission mechanism is related to the presence of a jet rather than accretion (e.g., Fossati et al. 1998; Ghisellini et al. 2017).

We conclude that Mrk 421 is not a binary candidate, according to our selection criteria, while Mrk 915 deserves a closer look at its light curve.
4.2. Light-Curve Analysis of Mrk 915

As reported in the previous section, the variability pattern of Mrk 915 possibly includes a periodic component with frequency $f_0 = 11 \pm 2 \text{ nHz}$, corresponding to a period of $P_0 = 35^{+5}_{-3} \text{ months}$ (see Figure 6). However, the g-test does not allow us to assess an absolute statistical significance, since it is tested near the boundary condition (see Protassov et al. 2002 for details), so it is only used to screen potential interesting candidates in our work. Moreover, the g-test does not take the photometric errors into account and, therefore, if the errors are large, i.e., their excess variance is small or negative, the periodicity might be apparent and must be tested with other methods. In the specific case of Mrk 915, the excess variance is negative, which implies that the observed variability could be apparent, and hence the PSD analysis must be handled with care and the putative periodicity should be investigated further.

In order to investigate this and to take the errors into account we first attempt a simple weighted least-squares sinusoidal fit of the light curve.\(^{18}\) The fitted function is given by $y(t) = A_0 + A_1 \sin(2\pi P_0^{-1}(t - t_0))$, where $A_0$, $A_1$, $t_0$, and $P_0$ are all free parameters. We obtain the following best-fit values, with errors given at a 90% confidence level:

$A_0 = (10 \pm 2) \times 10^{-4} \text{ cps}$

$A_1 = (5 \pm 2) \times 10^{-4} \text{ cps}$

$t_0 = 53 \pm 3 \text{ months}$

$P_0 = 35 \pm 2 \text{ months}$.

The goodness of fit is given by $\chi^2 /= \text{dof} = 82/96$. In Figure 7 we show the Swift-BAT light curve, overlapped by its best-fit sinusoidal curve. We note that the best-fit value of $P_0$ is consistent with the corresponding value of the PSD peak that is found with the g-test sample screening.

We use this latter result to perform a phase folding procedure on the light curve of Mrk 915 (e.g., Leahy et al. 1983). The epoch folding search is typically used to determine the period and the amplitude of the sinusoidal trend (see, e.g., Leahy 1987). However, given the short effective exposure time and the large period ($P_0 \approx 35$ months), it is not possible to oversample the Fourier resolution ($\Delta f = 1/\Delta t_{\text{exp}}$). Therefore, we use $P_0$ as a known parameter to fold the data set with $n = 6$ phase bins and test the null hypothesis. The number of bins is chosen as a trade-off between a high signal-to-noise ratio for each bin and the fact that significance tests, such as the $\chi^2$ test, are more reliable with more data points available.

We first compute the relative phase of each monthly observation as

$$
\phi = \frac{t}{P_0} - \text{int}\left(\frac{t}{P_0}\right),
$$

where $t$ is the time relative to the points of the light curve shown in Figure 7, and $\text{int}(a)$ is the integer part of $a$. We then combine the count rates corresponding to all points belonging to the same phase bin with the relative $1\sigma$ uncertainty. Given a set of $N$ observations with count rate $x_i \pm \delta x_i$ and exposure $\delta t_i$,
the count rates are combined as their weighted mean

$$X_{\text{bin}} = \frac{\sum_{i=1}^{N} x_i \left( \frac{1}{\delta x_i} \right)^2}{\sum_{i=1}^{N} \left( \frac{1}{\delta x_i} \right)^2},$$

while the errors are given by

$$\delta X_{\text{bin}} = \frac{1}{\sqrt{\sum_{i=1}^{N} \left( \frac{1}{\delta x_i} \right)^2}}.$$ 

This procedure is repeated for all the six phase bins we divide the period into. The folded light curve is shown in Figure 8.

To confirm the presence of a periodic trend, we test the null hypothesis with a $\chi^2$ test on the folded light curve, obtaining $\chi^2 \approx 24$, corresponding to a $p$-value of $2.3 \times 10^{-4}$ for 5 degrees of freedom (i.e., six phase bins minus one), which means that we are able to reject the null hypothesis with a confidence level of $3.7\sigma$.

5. Light-Curve Analysis of MCG+11-11-032

As shown in Section 4, our method only selects one SMBHB candidate from the AGN sample. It must be stressed, though, that the method is very conservative, and aims at selecting only the strongest candidates. Indeed, the only previously X-ray-selected SMBHB candidate (Severgnini et al. 2018), the Seyfert 2 galaxy MCG+11-11-032, is included in our Swift-BAT sample, but is excluded with the $g$-test selection criteria. It must be noted that the $p$-value threshold is low because we do not consider in this work periodicities with significance below $1/N_{\text{sources}}$. This does not mean that a periodic trend, which may be hidden by the noise, or hidden by large measurement errors, is not present. As shown in Figure 9, the highest value of the PSD is found at $f_0 = 15 \pm 2$ nHz, which corresponds to $P_0 = 26.3 \pm 0.6$ months, with $p_{\text{val}} > 0.0018$, i.e., not significant. The PSD slope is given by $\alpha = 0.4 \pm 0.3$ and is therefore consistent with white noise at a 90% confidence level. However, this Seyfert 2 galaxy was identified as a possible SMBHB candidate by means of the presence of two Fe Kα emission lines at energies $E = 6.16 \pm 0.08$ keV and $E = 6.56 \pm 0.15$ keV, at $4\sigma$ and $2\sigma$ confidence levels, respectively. Such lines, if emitted by two separate sources in the center of the AGN, would imply that they are red- and blueshifted Fe Kα emission lines by two minidisks, orbiting each other with a period of $P_0 \sim 25$ months.

The possible presence of a double Fe Kα emission line justifies an exception on the PSD screening and further investigation of this source. Therefore, we analyze the light curve of MCG+11-11-032, using the same procedure as that used for Mrg 915. We perform a weighted sinusoidal fit, testing again the function $y(t) = A_0 + A_1 \sin(2\pi P_0^{-1}(t - t_0))$. The best-fit values, with errors given at a 90% confidence level, are

- $A_0 = (5.8 \pm 0.9) \times 10^{-4}$ cph
- $A_1 = (2 \pm 1) \times 10^{-4}$ cph
- $t_0 = 63 \pm 3$ months
- $P_0 = 26.3 \pm 0.6$ months,

with a goodness of fit of $\chi^2/\text{dof} = 104/101$. The period derived is in agreement with the estimate given by Severgnini et al. (2018). Furthermore, in this case the period found with the sinusoidal fit is similar to the period corresponding to the maximum value of the PSD (Figure 9).

To further investigate MCG+11-11-032, we use the procedure adopted in Section 4.2 to perform epoch folding of the light curve of MCG+11-11-032, adopting six phase bins (red points in Figure 10). Also in this case we test the null hypothesis using a $\chi^2$ test, obtaining $\chi^2 \approx 15$, which corresponds to a $p$-value of $p_{\text{val}} = 0.0097$ for 5 degrees of
freedom. This means that the null hypothesis is rejected at the 2.6σ confidence level.

Assuming that the double Fe Kα spectral feature and the sinusoidal trend are the result of two different experiments of the same physical scenario, i.e., the presence of an SMBHB system, we use the meta-analysis technique called Fisher’s combined probability test (Mosteller & Fisher 1948). Given k independent experiments, each resulting in its own p-value $P_{val, i}$, the test consists in computing the following statistic:

$$X^2_{2k} = -2 \sum_{i=1}^{k} \ln(P_{val, i}),$$

where $X^2_{2k}$ is distributed as a $\chi^2$ with $2k$ degrees of freedom, and can be therefore tested as such. Since in our case $k = 2$, we test against a $\chi^2$ distribution with 4 degrees of freedom. In Severgnini et al. (2018) a significance of 2σ ($P_{val} = 0.05$) was reported for the least significant emission line. Using Equation (2) to combine such a p-value with the one obtained with the epoch folding we obtain $X^2_2 = 15.3$, corresponding to a global combined p-value of $P_{val} = 0.0042$ for 4 degrees of freedom. This means that, under the assumption that the spectral emission lines and the periodicity are both caused by the presence of a binary system, we are able to reject the null hypothesis of non-binarity with a 2.9σ confidence level.

As shown in Figure 10, the M-shape of the epoch folding plot suggests the possible presence of two harmonics. We add a second harmonic component to the fitting model, i.e., we fit the function $y(t) = A_0 + A_1 \sin(2\pi P_0^{-1}(t - t_0)) + A_2 \sin(4\pi P_0^{-1}(t - t_0))$. We find a goodness of fit of $\chi^2/\text{dof} = 101/99$, with an improvement given by $\Delta \chi^2/\text{dof} = 3/2$, meaning that the addition of the second harmonic is not significantly required by the data. However, we note that the best-fit period, $P_0 = 25.9 \pm 1.5$ months, is consistent with the ones found by fitting only one sinusoidal component. A longer light curve, possibly with a lower noise level, would be required to confirm the presence of a possible second harmonic component.

For this source, we also consider the 123 month 15–150 keV Palermo Swift-BAT light curve (Segreto et al. 2010), available only for this AGN, which was already presented in Severgnini et al. (2018) (Palermo Swift-BAT team, private communication). Assuming the derived period of ~26 months, this longer light curve samples almost five periods and could in principle return a higher significance for rejecting the null hypothesis. We bin the light curve at 5 months of observations per data point, to maximize the signal-to-noise ratio. The curve is well fitted by a single sinusoid $y(t) = A_0 + A_1 \sin(2\pi P_0^{-1}(t - t_0))$, with a goodness of fit of $\chi^2/\text{dof} = 17/19$, and a best-fit period $P_0 = 26.0 \pm 0.6$ months, consistent with the best fit obtained with the 105 month light curve. We use such a period to undertake the epoch folding technique, shown in Figure 10 (black points). We test the null hypothesis with a $\chi^2$ test, obtaining $\chi^2 \approx 21$, which corresponds to $P_{val} = 7.5 \times 10^{-4}$, implying that for this longer light curve the null hypothesis can be rejected at the 3.4σ confidence level. Considering also the result in Severgnini et al. (2018) in the combined probability test (Equation (2)), we obtain $P_{val} = 4.2 \times 10^{-4}$, which means that the null hypothesis can be rejected with a 3.5σ confidence level. The black points in Figure 10 also suggest in this case the presence of a second harmonic. However, adding a second harmonic component in the light-curve fit still produces a consistent period ($P_0 = 26.1 \pm 0.8$ months), but the goodness of fit is $\chi^2/\text{dof} = 12.6/17$; hence the second harmonic is required by the F-test at only the 93% confidence level.

6. Discussion and Conclusions

We have presented a method for selecting SMBHB candidates using Fisher’s exact g-test, finding a candidate in the Seyfert 1.5 galaxy Mrk 915 with a period given at the maximum value of the PSD of $P_0 = 35 \pm 2$ months. This source is not affected by colored noise, since the slope of its PSD is given by $\alpha = -0.4 \pm 0.3$, implying almost completely white noise, and there is only a 6% probability of the periodicity being a false positive. As a follow-up to this selection, we perform a sinusoidal fit on the Swift-BAT hard X-ray light curve spanning 105 months, and we find a period of $P_0 = 35 \pm 2$ months, consistent with the period corresponding to the maximum PSD value, with a goodness of fit of $\chi^2/\text{dof} = 82/96$. Furthermore, we test such a period with an epoch folding procedure, finding that the null hypothesis can be rejected with a 3.7σ confidence level. Assuming a Keplerian orbit, the distance $a$ between the two X-ray-emitting regions that embed the two SMBHs can be inferred by using Kepler’s third law, i.e., $a = (\text{GMP}_0^2/4\pi^2)^{1/3}$, where $M$ is the total mass of the two black holes, $P_0$ is the measured period, and $G$ is the gravitational constant. We adopt the black hole mass estimate $M = (1.1 \pm 0.4) \times 10^8 M_\odot$, computed using single-epoch Hβ measurements (Bennet et al. 2006). We derive a distance between the two hard X-ray-emitting regions of $a = (5 \pm 1) \times 10^{-3}$ pc. Assuming a circular orbit, the relative velocity between the putative black holes is $\Delta v = 2\pi aP_0^{-1} = (3.4 \pm 0.7) \times 10^{-2}c$. Previous X-ray

![Figure 10. Phase folding of the MCG+11-11-032 hard X-ray light curve. The folding period is divided into six phase bins. The gray points are copies of the six main bins, in order to highlight the periodic behavior. The red points are the result of the epoch folding of the 105 Month Swift-BAT survey light curve, while the black points represent the folding of the Swift-BAT 123 month long light curve, in the $E = 15–150$ keV energy band. The two curves have different count rates, because of different normalizations (see Segreto et al. 2010; Baumgartner et al. 2013, for further details).](image-url)
spectroscopy analyses of the source (e.g., Severgnini et al. 2015; Ballo et al. 2017) have not unveiled any double Fe Kα feature. In particular, XMM-Newton, with its energy resolution of ∼0.15 keV at the line energy, detects a single Fe Kα line at $E = 6.42 ± 0.02$ keV with no double peaks (Ballo et al. 2017). We can therefore conclude that, if the binary system is able to produce a double peak, the energy separation between the two peaks would be $\Delta E \lesssim 0.15$ keV. Given the orbital velocity $\Delta v$ obtained from the measured period, the expected Fe Kα energy shift is given by $\Delta E (\text{keV}) = E_{\text{Fe Kα}} \Delta v/c \approx 0.2 \sin \iota$, where $E_{\text{Fe Kα}} \approx 6.4$ keV and $\iota$ is the inclination angle. Since XMM-Newton only observes one emission line, if two peaks are indeed present in the X-ray spectrum, with $\Delta E \lesssim 0.15$ keV, this would mean that the inclination angle is $\iota \lesssim \pi/4$.

Alternatively, if the source is indeed able to produce double Fe Kα lines with energy separation above $\Delta E \sim 0.15$ keV, the two black holes could have been observed in a state in which they are aligned and hence the radial component of the velocity could be negligible. However, this is highly unlikely since the source has been observed more than once by Swift-XRT, Suzaku and XMM-Newton at epochs that are not spaced by half periods, and in none of these observations has a possible double Fe Kα line been detected, which precludes the aligned black hole hypothesis.

Given that MCG+11-11-032 was reported as a possible binary SMBH by Severgnini et al. (2018), we also analyze the light curve of this Seyfert 2 galaxy, finding a best-fit period of $P_0 = 26.3 ± 0.6$ months, with a goodness of fit of $\chi^2$/dof = 104/101. By visual inspection, Severgnini et al. (2018) gave a rough estimate of the period of $P_0 \sim 25$ months, which is likely to be consistent with our result. From the SMBH mass of Lamperti et al. (2017), $\log(M/M_\odot) = 8.7 ± 0.3$, derived from the velocity dispersion of the CO molecules, we infer that the separation of the two black holes is $a = \left[\frac{GMP_0^2}{4\pi^2}\right]^{1/3} = (6.5 ± 1.5) \times 10^{-3}$ pc, from which we can quickly compute $\Delta v = 2\pi a P_0^{-1} = (0.06 ± 0.02)c$. We expect an energy shift of $\Delta E = E_{\text{Fe Kα}} \Delta v/c = 0.38 ± 0.02$ keV, assuming an inclination angle $\iota = \pi/2$, typically adopted for Seyfert 2 sources, and assuming that the orbital plane of the black holes is aligned with the AGN inclination. This result is highly consistent with the observed centroid energies of the two Fe Kα lines, found in Severgnini et al. (2018) at $E_1 = 6.16 ± 0.08$ keV and $E_2 = 6.56 ± 0.15$ keV, i.e., $\Delta E = 0.4 ± 0.2$ keV. This strongly supports the hypothesis that the observed double-peaked Fe line and periodicity are both produced by the same physical effect, likely to be the presence of two SMBHs in close orbit around each other. Hence, it is reasonable to consider our result (based on the Swift-BAT light curve) and the Severgnini et al. (2018) result (based mostly on the double Fe K line in Swift-XRT data) as the results of two independent experiments of the same physical scenario; this allows us to combine the two $p$-values (see Section 5) and reject the null hypothesis at the combined confidence level of 2.9$\sigma$. The results for Mrk 915 and MCG+11-11-032 are summarized in Table 1.

We note that the observed periodicity, in principle, may be produced by the circumbinary disk periodic accretion flow into the cavity, or by the modulated emission by the minidisks, which has the same period as the binary. However, as argued by Tang et al. (2018), the circumbinary emission is dominant in soft X-rays ($E < 4–5$ keV), while in hard X-rays, including the BAT energy band, the observed emission is dominated by the minidisk emission. Moreover, concerning MCG+11-11-032, the consistency between the observed energy shift between the two Fe Kα emission lines and the expected one inferred from the periodicity strongly favors the minidisk scenario. This means that the observed periodicity is likely to be the same as that of the binary system.

Both Mrk 915 and MCG+11-11-032 would likely emit continuous GWs with gravitational frequencies $f_{gw} = 2/P_0 \approx 22$ nHz and $f_{gw} \approx 30$ nHz, respectively, close to the frequency where PTAs are most sensitive (e.g., Lentati et al. 2015; Moore et al. 2015; Shannon et al. 2015; Mingarelli et al. 2017; Arzoumanian et al. 2018). However, current PTA data sets are not sensitive enough for any of these two sources, since GW signals from a single source can currently be observed only for sources with $\log(M/M_\odot) \gtrsim 9.2$ at a distance of $d \lesssim 150$ Mpc (Aggarwal et al. 2019). Therefore, the GWs emitted by both Mrk 915 and MCG+11-11-032 would be significantly below the current detection limit of PTAs.

While waiting for the first PTA detection and the improvement of the sensitivity curve, we find X-rays are a very promising tool for discovering possible SMBHBs. Longer light curves are required for two main reasons: (i) to confirm current candidates with a higher significance. Note that the current 105 month Swift-BAT data release samples only approximately three periods for Mrk 915 and only nearly four for MCG+11-11-032. For the latter, the 123 month data set has significantly improved detection, from 2.6$\sigma$ to 3.4$\sigma$. The greater the number of data points we combine for each phase bin (see Section 4.2), the smaller the errors on the epoch folding, which results in a much better $\chi^2$ test. (ii) To find new candidates with the PSD selection criteria described in Section 4. In fact, by sampling longer continuous periods, while the noise level at a given frequency remains roughly constant, the periodic peak, if present, will be much higher at any additional sampled period. Longer Swift-BAT light curves, which will allow us to study the variability for up to $\sim 250$ months, will therefore be crucial for periodicity studies. Additionally, the Wide Field Monitor on board the future Enhanced X-Ray Timing and Polarimetry Mission (Zhang et al. 2019) may continue the legacy of BAT even after the decommissioning of the Swift telescope.

Table 1

| Source Name | Type | Identified as Candidate | Period (months) | $\chi^2$ p-value | $d_s$ (Mpc) | $a$ ($10^{-3}$ pc) | $\Delta v/c$ |
|-------------|------|------------------------|----------------|-----------------|------------|-------------------|------------|
| Mrk 915     | Seyfert 1.5 | This paper | 35 ± 2 | $2.3 \times 10^{-4}$ | 105 | 5 ± 1 | 0.034 ± 0.007 |
| MCG+11-11-032 | Seyfert 2 | Severgnini et al. (2018) | 26.3 ± 0.6 | $9.7 \times 10^{-3}$ | 160 | 6.5 ± 1.5 | 0.06 ± 0.02 |

Note. We report the name of the source, the AGN type, the reference where it was first reported as a candidate SMBHB, the period obtained with a sinusoidal fit in units of months, the epoch folding $p$-value obtained with a $\chi^2$ test of the null hypothesis, the luminosity distance of the AGN, the separation between the two black holes under the assumption that the observed periodicity is due to a binary system, and their relative velocity.

| Source Name | Type | Identified as Candidate | Period (months) | $\chi^2$ p-value | $d_s$ (Mpc) | $a$ ($10^{-3}$ pc) | $\Delta v/c$ |
|-------------|------|------------------------|----------------|-----------------|------------|-------------------|------------|
| Mrk 915     | Seyfert 1.5 | This paper | 35 ± 2 | $2.3 \times 10^{-4}$ | 105 | 5 ± 1 | 0.034 ± 0.007 |
| MCG+11-11-032 | Seyfert 2 | Severgnini et al. (2018) | 26.3 ± 0.6 | $9.7 \times 10^{-3}$ | 160 | 6.5 ± 1.5 | 0.06 ± 0.02 |

Note. We report the name of the source, the AGN type, the reference where it was first reported as a candidate SMBHB, the period obtained with a sinusoidal fit in units of months, the epoch folding $p$-value obtained with a $\chi^2$ test of the null hypothesis, the luminosity distance of the AGN, the separation between the two black holes under the assumption that the observed periodicity is due to a binary system, and their relative velocity.
It must be stressed that the present work does not represent a full statistical study of the SMBHB population in the local universe. First of all, it is limited to AGN, which are only \sim 10% of the SMBHs in the observable universe, and there is no reason to privilege active over non-active galaxies. Second, the selection criteria include only the most prominent peaks and exclude sources with periodicities buried under a high level of noise. This is clear in the case of MCG+11-11-032, which is excluded from the PSD selection given its high level of non-periodic noise. This is also true for the method used in Liu et al. (2020), in which a cut in excess variance has been applied, because the PSD does not take photometric errors into account, leaving both Mrk 915 and MCG+11-11-032 out of their sample. However, we note that we obtain the same results in the coincident sample, even if the two methods are different. Moreover, concerning MCG+11-11-032, we stress that we are able to reject the null hypothesis above 3\sigma only when we consider the 123 month long light curve, which samples around 123 noise. This is clear in the case of MCG+11-11-032. Finally, the detection of double-peaked Fe Kα lines is still in its pioneering stage. XMM-Newton, currently the instrument with the largest effective area in the Fe Kα spectral region, is only able to observe energy shifts \Delta E \gg 0.15 keV. Therefore, double Fe lines produced by orbital motions of SMBHBs with the range of periods analyzed in this work is only observable for a limited number of AGN, mostly those with edge-on inclinations. Future microcalorimeters such as the ones on board XRISM (e.g., XRISM Science Team 2020) and Athena (e.g., Barret et al. 2016) will revolutionize the search for binary SMBHs, being able to detect energy shifts down to \Delta E \sim 0.01 keV, and possibly opening the window for the search for double-peaked Fe Kα lines in many more Seyfert galaxies and quasars.

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