Characterizing Scalability of Sparse Matrix-Vector Multiplications on Phytium FT-2000+ Many-cores

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Abstract Understanding the scalability of parallel programs is crucial for software optimization and hardware architecture design. As HPC hardware is moving towards many-core design, it becomes increasingly difficult for a parallel program to make effective use of all available processor cores. This makes scalability analysis increasingly important. This paper presents a quantitative study for characterizing the scalability of sparse matrix-vector multiplications (SpMV) on Phytium FT-2000+, an ARM-based HPC many-core architecture. We choose SpMV as it is a common operation in scientific and HPC applications. Due to the newness of ARM-based many-core architectures, there is little work on understanding the SpMV scalability on such hardware design. To close the gap, we carry out a large-scale empirical evaluation involved over 1,000 representative SpMV datasets. We show that, while many computation-intensive SpMV applications contain extensive parallelism, achieving a linear speedup is non-trivial on Phytium FT-2000+. To better understand what software and hardware parameters are most important for determining the scalability of a given SpMV kernel, we develop a performance analytical model based on the regression tree. We show that our model is highly effective in characterizing SpMV scalability, offering useful insights to help application developers for better optimizing SpMV on an emerging HPC architecture.

Keywords SpMV · Many-Core · Scalability · Performance Modeling

1 Introduction

Multi-core and many-core architectures offer the potential of delivering scalable performance through parallelism. Realizing such potential is, however, not trivial due to multiple factors, including available application parallelism, limited working sets, and communication overheads. Among these factors, the share memory resources, such as shared caches, is often a performance bottleneck for many application domains due to memory contention [23].

The memory bandwidth is increasingly becoming a limiting factor for the high-performance computing (HPC) domain. On the one hand, there are more and more processor cores that are integrated into a single chip, to provide more computation power. On the other hand, using a larger number of processor cores is likely to raise memory contention and increase the pressure on the memory bus. As a result, it is not always beneficial to use a large number of cores even if abundant parallelism is available [17]. To unlock the potential of multi- and many-core architectures and to justify the further specialization of processor design, it is important to understand the impact of the shared memory resources on application scalability.

In this paper, we present a quantitative approach to characterize the scalability of sparse matrix-vector multiplications (SpMV) on HPC many-core architectures. SpMV is one of the most common operations in scientific and HPC applications [39]. It is highly challenging to optimize SpMV on parallel architectures [50], due to several reasons like irregular indirect data accessing, sensitivity to the sparsity pattern of the input matrix, and the subtle interaction of the matrix storage format, the problem size, and hardware. While there is considerable work on finding the right sparse matrix storage format [4], little effort has been spent
on characterizing and understanding the scalability of SpMV on multicore architectures. As the HPC hardware is firmly moving towards many-core design, it is crucial to know when it is beneficial to use the available cores and how the SpMV performance will scale as we increase the number of cores to use.

Our work specifically targets the ARMv8-based Phytium FT-2000+ many-core architecture. Because ARM-based processors are emerging as an interesting alternative building block for HPC systems [20, 40, 52], it is important to understand how the hardware microarchitecture design affects the SpMV scalability. Having such knowledge is useful not only for better utilizing the computation resources, but also for justifying a further increase in the processor core provision on a single chip.

In this work, we conduct a comprehensive evaluation and analysis to study the scalability of SpMV on the latest FT-2000+ many-core. Our study mainly targets the Compressed Sparse Row (CSR) storage format. We choose CSR because it is a widely used representative storage format for sparse matrices in scientific computing. Since there are many variations of the CSR format, our optimization has great practical significance and can easily be extended to other CSR-extended formats.

Our experiment shows that despite many SpMV applications contain extensive parallelism, they often fail to achieve a linear speedup on FT-2000+. To characterize what affects the scalability of SpMV, we collect extensive profiling information (through hardware performance counters) from a large-scale experiment involved over 1,000 representative sparse datasets. With this extensive set of profiling data in place, we develop a regression-tree based analytical model to capture what information is useful for reasoning about the scalability of SpMV. We show that our analytical model is highly accurate in revealing what affects the SpMV scalability on FT-2000+. We demonstrate that our model can provide useful insights to guide the application developers to better optimize SpMV on an emerging ARMv8-based many-core architecture.

To summarize, this paper makes the following contributions. It is the first to

- characterize the scalability performance of SpMV on FT-2000+, an emerging ARMv8-based many-core architecture for HPC;
- use machine learning techniques to correlate and analyze how hardware micro-architecture features affect the SpMV scalability;
- show how machine learning can be used to develop a performance profiling tool to guide the optimization of SpMV on ARM-based HPC architectures.

2 Background and Motivation

In this section, we first introduce the SpMV and its sparse matrix storage formats and then explain the motivation of this work.

2.1 Sparse Matrix-Vector Multiplication

A SpMV operation can be defined as \( y = Ax \) where the input is a sparse matrix \( A (m \times n) \) and a dense vector \( x (n \times 1) \), and the output is a dense vector \( y (m \times 1) \).

Figure 1 shows an illustrative example of SpMV, where \( m = n = 4 \), and the nonzeros \( nnz = 8 \).

2.2 Sparse Matrix Storage Formats

In our work, we mainly consider the SpMV based on CSR, the most commonly used format for storing sparse matrices, and its improved counterpart, CSR5 [24]. The example matrix mentioned above in these two formats is shown in Table 1.

CSR. The compressed sparse row (CSR) format explicitly stores column indices and nonzeros in arrays indices and data, respectively. It uses a vector ptr, which points to row starts in indices and data, to query matrix values. The length of ptr is \( n_{row} + 1 \), where the last item is the total number of the nonzero elements of the matrix.

CSR5. The CSR5 format aims to obtain a good load balance for matrix value queries [24]. It achieves this by partitioning all nonzero elements into multiple 2-dimensional tiles of the same size, corresponding to the width and the height of the tile respectively. Later in this paper, we show how CSR5 gain better scalability than CSR by more uniform and reasonable task assignment in multi-threaded SpMV.
Table 1 The sparse matrix storage formats targeted in this work and the corresponding data structures for the example shown in Figure 1.

| Representation | Specific Values |
|----------------|-----------------|
| CSR            | $\text{ptr} = [0, 2, 5, 6, 8]$  |
|                | $\text{indices} = [1, 2, 0, 2, 3, 2, 1, 2]$  |
|                | $\text{data} = [5, 2, 6, 8, 3, 4, 7, 1]$  |
| CSR5           | $\text{ptr} = [0, 2, 5, 6, 8]$  |
|                | $\text{tile}_{\text{ptr}} = [0, 1, 4]$  |
|                | $\text{tile}_{\text{des}} : \text{bit}_{\text{flag}} = [T, T, F, F, T, T, T, F]$  |
|                | $\text{y}_{\text{off}} = [0, 1, 0, 2]$  |
|                | $\text{seg}_{\text{off}} = [0, 0]$  |
|                | $\text{indices} = [1, 0, 2, 2, 3, 1, 2, 2]$  |
|                | $\text{data} = [5, 6, 2, 8, 3, 7, 4, 1]$  |

Fig. 2 Performance comparison of SpMV on two multicore processors. The x-axis represents the number of threads and the y-axis represents the obtained performance (in Gflops).

2.3 Motivation

We run the multi-threaded SpMV in CSR on a x86-based Xeon multi-core (Intel Xeon E5-2692) and a ARMv8-based Phytium multi-core (FT-2000+). Figure 2 shows the SpMV performance for the bone010 dataset when using threads ranging from 1 to 16.

We observe that, on Xeon the speedup increases linearly when using 1 thread up to 4 threads, while the performance increase is very slight when using further-more threads. At this moment, the SpMV performance on Xeon is limited by the off-chip memory accesses. By contrast, the SpMV scalability is rather different on FT-2000+. We see a very slight performance increase when using 1, 2, and 4 threads. Thereafter, we notice a quasi-linear speedup until using 16 threads. We believe that these performance behaviours are determined by the interactions of the SpMV code, the input sparse matrix, and the underlying micro-architecture. In this work, we will look into the factors which impact the SpMV scalability on FT-2000+.

Given that the performance ‘odds’ appear when using fewer than 8 threads, we will focus on scalability characterization on a core-group within a panel of FT-2000+ (see Figure 3 and Section 3).

3 Experimental Setup

In this section, we will introduce the hardware platforms, the installed system software, and the datasets used in this work.

Hardware Platforms. As depicted in Figure 3, FT-2000+ integrates 64 ARMv8 based Xiaomi cores. Its Mars II microarchitecture offers a peak performance of 588.8 Gflops for double-precision operations, with a maximum power consumption of 96 Watts. The CPU chip has eight panels with eight 2.3GHz cores per panel. Each core has a private 32KB L1 data cache, and a 2MB L2 cache is shared among four cores (core-group). The panels are connected through two directory control units (DCU) [1].

Systems Software. We run a customized Linux OS with Linux Kernel v4.4 on FT-2000+. For compilation, we use gcc v6.4.0 with the “-O3” compiler option. We use the OpenMP threading model, using 1-4 threads on FT-2000+. Datasets. We use 1008 square matrices (with a total size of 80 GB) from the SuiteSparse matrix collection [10]. The number of nonzero elements of the matrices ranges from 100K to 200M [22]. The dataset includes both regular and irregular matrices, covering domains from scientific computing to social networks [25].
4 SpMV Scalability Results and Modelling

In this section, we show the overall scalability performance of SpMV. To identify the impacting factors of SpMV scalability on FT-2000+, we build a regression-tree based model, which automated relates features to speedup (normalized to a single thread). We use key features collected from hardware performance events and the input sparse matrix datasets.

4.1 Overall Performance Results

Figure 4 shows the overall speedup of SpMV with 1-4 threads on a core-group of FT-2000+. The x-axis represents different sparse matrices. Although the achieved speedup for most matrices increases over the number of threads, we note the performance is far less than the linear speedup. Most speedup numbers lie between 1 and 2, and a very small portion of numbers are beyond that. Also, the obtained speedup is hyper-linear for some datasets. This is because the dataset is so small that it can be hold within the shared L2 data cache. Table 2 shows a statistical profile of the average speedup when using multiple threads (normalized to a single thread). We use key features collected from hardware performance events and the input sparse matrix datasets.

Table 2 The average speedup(x) of SpMV with multi-threads over a single-thread.

| #threads | speedup |
|----------|---------|
| 1        | 1.0x    |
| 2        | 1.50x   |
| 3        | 1.77x   |
| 4        | 1.93x   |

4.2 Scalability Modelling

To find the impacting factors for scalability, we use an empirical approach to manually analyze the performance behaviours. As an alternative, we use a machine-learning based approach to build a model and then let the model tell us which feature plays a role in scaling SpMV on FT-2000+. Instead of hand-crafting an analytical model that requires expert insight into low-level hardware details, we employ machine learning techniques to automatically learn the correlation between features and the SpMV (speedup) performance.

Building and using the regression tree model follows three main steps: (i) generate training data, (ii) train a regression model, and (iii) find the factors with a large weight. Given that our model is used as a tool for analysis rather than for predicting the speedup of SpMV, we make the best use of the collected data by selecting 90% samples for training, instead of the usual (80%, 20%) data splitting between model training and model testing.

4.2.1 Collecting Training Data

To generate training data for our model, we used 1008 sparse matrices from the SuiteSparse matrix collection. We run the CSR-based SpMV a number of times until the gap of the upper and lower confidence bounds is smaller than 5% under a 95% confidence interval setting. The code is run with 1, 2, 3, and 4 threads, with each pinned to a fixed core. We then record the SpMV execution time for computing speedup (normalized to a single thread) and obtain hardware performance counters by using PAPI (Performance Application Programming Interface [41]) for each training sample. As the last step, we collect key values for each input dataset to capture its features.

Table 3 shows our selected features from both sparse matrix structure and hardware events. These important matrix features introduced in [5] are proved to be effective in capturing the spatial patterns of the matrix. The raw hardware counters we collected are related to performance [28]. To improve the model performance, we calculate a set of derived features based on raw counter values and use them as the input of the model. There are two customized features: \( L2_{DCMR\_change} \) and \( job\_var \). The former indicates the changes of \( L2_{DCMR} \) from one to four threads. As for the \( L2_{DCMR} \) with four threads, we use the \( L2_{DCMR} \) on the slowest thread instead of the total one; the \( job\_var \) represents the degree of nonzero distribution imbalance across threads (the theoretical value is 0.25 for 4 threads).
Table 3 The selected features and their descriptions.

| Features                  | Description                                      |
|---------------------------|--------------------------------------------------|
| n_rows                    | number of rows                                   |
| nnnz_max                  | maximum # nonzeros per row                       |
| nnnz_avg                  | average # nonzeros per row                       |
| nnnz_var                  | variance # nonzeros per row                      |
| L2_DCM                    | L2 data cache misses                             |
| L2_DCA                    | L2 data cache accesses                           |
| L1_DCM                    | L1 data cache misses                             |
| L1_DCA                    | L1 data cache accesses                           |
| FR_INS                    | floating point instructions executed             |
| TOT_INS                   | total instructions executed                      |
| TOT_CYC                   | total cycles                                      |
| L2_DCMR                   | L2 data cache miss rate                          |
| L2_DCMR_change            | the change of L2_DCMR                            |
| job_var                   | maximum # allocated nnz ratio per thread          |

4.2.2 Building The Model

For simplicity, we only use performance counters collected when using one thread and four threads. The achieved speedup and the corresponding feature set is taken as the input of the supervised learning algorithm built in scikit-learn. The learning algorithm tries to find a correlation between the features, performance values and achieved speedups. The output of this training process is a regression-tree based model, which helps to reveal the factors that affect SpMV scalability.

4.2.3 Identifying the Impacting Factors

By using the feature importance module of scikit-learn for the new-built regression tree model [34], we can obtain the top three factors that most affect the SpMV scalability: the nonzero allocation, the shared L2 cache, and the nnz variance across rows, where nnz denotes the number of nonzero. Figure 5 shows how these factors impact the SpMV speedup. In the next section, we will give a detailed analysis of the scalability with our trained model.

5 Scalability Analysis, Insights and Optimizations

In this section, we first examine how individual factor suggested by the model (Section 4.2.3) impacts the SpMV speedup. We then conduct an in-depth analysis of how the factors have an impact on the SpMV scalability with four representative matrices. We choose the four datasets because their speedups are mainly limited by separate factors. At last, we introduce several potential optimizations inspired by the scalability results.

Fig. 5 A tree picked from the regression forests intuitively shows how the factors impact the speedup of SpMV.

5.1 SpMV Scalability Factors

Based on the data obtained from executing SpMV on datasets, we draw scatter plots between each impacting factor and the speedup, which are shown in Figure 6. It is clear that the speedup generally shows a gradual decline trend when the nonzero allocation across threads becomes more unbalanced, the L2_DCMR increases from one thread to four threads, or the nonzero variance of sparse matrices go larger.

The three bar charts in Figure 6 show the statistical results of integral histogram of the speedup results, which is consistent with the results in the left part of Figure 6. There are also some cases that do not meet our expectations. For example, Figure 6(d) shows that the speedup even decreases when L2_DCMR_change is less than 0. We argue that it is a comprehensive product of multiple impacting factors, which needs further investigation. In this following, we will analyze how each factor has an impact on the SpMV scalability.
The balance of the nonzero allocation. When running the conventional SpMV code in the CSR format, the nonzero allocation across threads depends on the sparse matrix structure. As shown in Figure 6(b) when job\_var is greater than 0.45, which means that the nonzeros are clustered within some rows to be dispatched to a specific thread, load imbalance will occur and this thread will take substantially more time than the other threads. Thus, the unbalanced nonzero allocation among threads will put a limit on the achieved speedup, because the SpMV performance is determined by the slowest thread.

Taking exdata\_1 in Table 4 for instance, the second thread will consume more than 99% of the nonzeros when using 4 threads, and thus the achieved speedup stays around 1.02x in such a case.

The shared L2 data cache. Leveraging shared resources on multi-core architectures improves the utilization of a hardware component and can improve overall system throughput. On the one hand, such a design as cache sharing can lead to positive interference, i.e., one thread brings data into the shared cache which is accessed by other threads [13]. The debr in Table 4 gives
Table 4 The concise description of four representative matrices.

| matrix    | job_var | L2_DCMR_change | nnz_var | sparsity structure | speedup |
|-----------|---------|---------------|---------|---------------------|---------|
| exdata    | 0.992   | 0.000         | 649.627 |                     | 1.018x  |
| conf5_4-8x8-20 | 0.250   | 0.056         | 0.000   |                     | 1.351x  |
| debr      | 0.250   | -0.001        | 0.003   |                     | 2.241x  |
| appu      | 0.252   | -0.001        | 36.494  |                     | 1.479x  |

an intuitive example for the benefits of shared memory. Recalling the SpMV algorithm, \( y = Ax \), where the dense vector \( x \) is the data structure to be reused across threads. This occurs because different threads deal with distinct matrix rows of \( A \), while \( x \) is shared by all threads. When running SpMV on \( \text{debr} \) with 4 threads on FT-2000+, with the L2 cache sharing within a core-group, threads[1, 3] and threads[2, 4] can share the dense vector \( x \) so as to increase the data reuse and improve the performance of multi-threaded SpMV.

On the other hand, cache sharing can have a negative impact on the per-thread performance from the perspective of resource competition. The L2 cache sharing on FT-2000+ may cause threads to evict data of other threads when running SpMV, which means that the ‘victim’ threads will experience more cache misses than their isolated execution. And we find that the degree of the negative impact from cache sharing is related to the average nonzeros per row (\( \text{nnz}_{\text{avg}} \)). In general, a larger \( \text{nnz}_{\text{avg}} \) leads to more competitions. We argue that this is because \( \text{nnz}_{\text{avg}} \) represents the need for dense vector \( x \) per row when running SpMV, which means that the data evicting increases as \( \text{nnz}_{\text{avg}} \) goes up. As shown in Figure 6(c), as \( \text{L2}_{\text{DCMR}} \) increases for most matrices, we note a corresponding decrease in speedup.

To summarize, we note that the impact of cache sharing on SpMV relates to specific input matrices and their structures. In Table 4, the SpMV gains a much larger speedup on \( \text{debr} \) (2.241x) than on \( \text{conf5_4-8x8-20} \) (1.351x) with 4 threads. On the one hand, the data reuse that benefits from the distribution of nonzeros makes contributions; on the other hand, the average nonzeros per row of \( \text{conf5_4-8x8-20} \) is larger than its counterpart (39 vs 4), which means that running SpMV on \( \text{conf5_4-8x8-20} \) generates more contention with shared L2 cache. These two reasons both lead to a higher increase on \( \text{L2}_{\text{DCMR}} \) of \( \text{conf5_4-8x8-20} \) than \( \text{debr} \) from one thread to four threads.

The nonzero variance across rows. The utilization of the dense vector \( x \) has a significant impact on the SpMV scalability. However, to obtain the correlation of nonzero distribution row by row is time-consuming for large-scale sparse matrices. As a result, we choose the nonzero variance across rows instead. This metric can reflect the regularity of input matrices and capture how the dense vector \( x \) will be reused.

Note that the speedup is calculated by dividing the single-thread execution time by the that of multiple threads, and the latter depends on the thread that spends the most time. Thus, an even distribution of the SpMV execution across threads typically leads to satisfactory SpMV scalability. However, we observe that the balanced nonzero allocation across rows does not necessarily lead to a large speedup like matrix \( \text{debr} \) listed in Table 4. This is because the different nonzeros distribution across rows (and threads) equally has an impact on the execution time. For \( \text{debr} \), despite the fact that nonzeros are evenly allocated across threads, the large \( \text{nnz}_{\text{var}} \) results in different reuse of vector \( x \), and leads to different execution behaviours across threads and an unsatisfactory speedup. As shown in Figure 6(f), matrices with smaller \( \text{nnz}_{\text{var}} \) tend to bring a larger speedup. This can be equally explained that a smaller nonzero variance across rows can ensure that the workloads can
be more evenly distributed and better exploit the locality of vector x.

5.2 Potential Optimizations

5.2.1 Using storage formats with balanced nonzero allocation

The load imbalance is mainly related to the adopted CSR format and the thread scheduling policy. In most cases, we use the static scheduling policy because the overhead of thread communication with dynamic scheduling is nonnegligible. To overcome the issue of load imbalance, we choose to use storage formats that divide nonzeros equally among threads. The CSR5 format is selected because it is designed to solve the load imbalance in CSR-based SpMV, and its data structure is shown in Section 2.2.

We choose matrices whose scalability suffers from load imbalance by its job var value (≥ 0.45), and then run CSR5-based SpMV on the matrices. The results show CSR5 achieves an average improvement of speedup from 1.632x to 2.023x. Figure 7 shows the performance result on exdata_1. Compared with the CSR format, load imbalance is significantly mitigated by running the CSR5-based SpMV with job var decreasing from 0.992 to 0.298. As a consequence, the speedup gains an improvement from 1.018x to 1.468x. CSR5 performs better because the nonzeros are divided and organized in small tiles instead of the row manner. Therefore, when dealing with irregular matrices, despite that the rows with a large number of nonzeros may be concentrated like exdata_1, they will not be assigned to the same thread. Thus, the workloads can be dispatched in a much more even manner across threads and improve the scalability of SpMV.

5.2.2 Avoiding the contention from shared memory resources

Based on the analysis in Section 5.1, we know that the sharing L2 cache of FT-2000+ has a great impact on the scalability of SpMV. Under most circumstances, the sharing cache causes more contention, which leads to a speedup decline. To alleviate the pressure from cache sharing, we bind threads to multiple cores that are located in different core-groups (Section 3). In this way, we can ensure that each thread occupies a complete L2 cache without data interference from other threads.

When running SpMV on all the matrices in the private-L2 mode, we can achieve a considerable average speedup of 3.40x on 4 threads, compared with 1.93x on one core-group (Table 2). As can be seen from Figure 8, the speedup with private L2 caches significantly outperforms its counterpart of sharing an L2 data cache on conf5_4-8x8-20, with a speedup increasing from 1.35x to 3.61x. This is because using private L2 caches can effectively reduce the L2 cache miss from 30% to 25%. But this approach of using a private L2 data cache will not bring a performance increase for all matrices. Taking another matrix asia_osm for example, the speedup only increases by 2.6% from 3.170x to 3.254x with private L2 caches. We reckon that the average nonzeros per row of this matrix is less than 3, so that the shared L2 cache can meet with their memory accessing need.

5.2.3 Exploiting locality-aware SpMV storage formats

Based on the aforementioned analysis, we know that merely achieving balanced nonzero allocation is insufficient, and the locality of x in SpMV needs to be exploited to achieve better scalability. Here is our idea to design a novel storage format that can make good use of the locality: we bring together the rows with a sim-
Fig. 9 The synthesized sparse matrix with poor locality utilization of the vector $x$ (left) and the corresponding matrix in ideal locality-aware SpMV storage format (right).

ilar nonzero distribution, so that the vector $x$ can be reused.

To explore the feasibility of designing the locality-aware SpMV storage format, we generate a series of matrices of different sizes as shown in Figure 9. This synthesized matrix has a poor locality of vector $x$ when running SpMV. And we then transform such matrices to locality-friendly forms by partial reordering. Table 5 shows the result of running CSR-based SpMV on a specific pair of matrices on FT-2000+. Both single-threaded and multi-threaded performance gain significant improvement. Particularly, the 64-thread performance improves by 71.7% from 15.907 Gflops to 27.306 Gflops. At the same time, better scalability of SpMV is achieved from 37.96x to 46.68x.

To conclude, we introduce several potential optimizations inspired by the scalability results, but these are not one-fit-all solutions. This is because there is an overhead for format conversion, and using multiple private L2 caches waste extra memory resources. For future work, we will extract a detailed profile of a given sparse matrix before performing the SpMV computation. Hopefully, these features will indicate the number and distribution of nonzeros. Based on this information, we can decide whether to apply these optimizations or not. Besides, we will try to find an accurate and efficient matrix reordering that can be applied to design the locality-aware SpMV storage format.

6 Related Work

Substantial previous work has been conducted to study the SpMV performance on parallel systems [7, 30, 33, 40]. Mellor-Crummey et. al use a loop transformation to improve the performance of SpMV on multiple parallel processors, and this optimization is aimed at the matrices that arise in SAGE [30]. Pinar et. al propose alternative data structures, along with reordering algorithms to reduce the number of memory indirections when running SpMV on a Sun Enterprise 3000 [35]. Williams et. al apply several optimization strategies especially effective for the multicore environment to SpMV on four multicore platforms. These works have a significant effect on improving the performance of parallel SpMV [50]. However, very few works focus on its scalability performance on many-core architectures. Our work fills this gap by providing an in-depth scalability analysis on FT-2000+. The obtained insights will facilitate us to design more efficient parallel HPC software and hardware in the future.

Efforts have been made in designing new storage formats for various parallel processor architectures including SIMD CPUs and SIMT GPUs [1, 19, 24, 27, 31]. Bell et. al use standard CUDA idioms to implement several SpMV kernels which can exploit fine-grained parallelism to effectively utilize the computational resources of GPUs, including SIMD-friendly ELL, the most popular general-purpose CSR and hybrid ELL/COO format that exploits the advantages of both [4]. The CSR5 proposed by Liu et. al is efficient both for regular matrices and for irregular matrices and is also used in our work to address the issue of unbalanced loads [24]. Maggioni et. al propose the design of an architecture-aware technique for improving the performance of the SpMV on GPU, and based on a variation of the sliced ELL sparse format, they present a warp-oriented ELL format that is suited for regular matrices [27]. The SELL-C-σ format is designed by Kreutzer et. al, and this SIMD-friendly data format is well-suited for a variety of hardware platforms (Intel Sandy Bridge, Intel Xeon Phi, and Nvidia Tesla K20) [19]. These sparse matrix formats aim to address the issue of unbalanced load and increase SpMV parallelism, but they fail to take advantage of the locality of vector $x$. Our work attempts to answer this question by providing comprehensive analysis and new insights.

A large number of works have analyzed the sources of poor scalability in various parallel applications, rather than SpMV [3, 11, 23]. Alam et. al propose an appropriate selection of MPI task and memory placement schemes to improve performance for key scientific calculations on multi-core AMD Opteron processors [3]. Liu et. al introduce the notion of memory access intensity to facilitate quantitative analysis of programs memory behavior on multicores [23]. For the work of Diamond et. al, it not only examines traditional unicores metrics and but also presents an in-depth study of performance bottlenecks originating in multicore-based systems. Besides, it introduces a source-code optimization called loop microfission to alleviate multicore-related performance bottlenecks [11]. Bhattacharjee et. al [6] predict critical threads, or threads that suffer from imbalance. They tend to offer more resources to critical threads so
that they run faster. Most of these related works focus on the traditional x86 multi-core architectures, and very few works are towards the ARMv8-based many-cores or the SpMV kernel, which is rather promising for the future of the HPC domain.

Numerous performance analysis tools have been proposed, including CounterMiner and HPCTOOLKIT [2, 26]. By using data mining and machine learning techniques, CounterMiner enables the measurement and understanding of big performance data [26]. HPCTOOLKIT can pinpoint and quantify scalability bottlenecks of fully optimized parallel programs. Based on statistical sampling, this tool can introduce with a very small measurement overhead during performance measurement [2]. Different from these performance tools, our regression-tree based approach uses both hardware counters (dynamic features) and input matrix features (static features), thus brings a comprehensive understanding of the scalability behaviours.

Other researchers have used performance counters to identify multicore bottlenecks and optimize applications [23], but no quantitative analysis is performed in those studies. Our work not only conducts detailed scalability analysis, but also is the first attempt in applying machine learning techniques to find the impact factors of SpMV scalability on FT-2000+.

Machine learning has quickly emerged as a powerful design methodology for systems modeling and optimization [13]. Prior works have demonstrated the success of applying machine learning for a wide range of tasks, including modeling code optimization [8, 9, 15, 21, 22, 23, 24, 25, 27, 31, 32, 33, 38, 42, 44, 45, 46, 47, 48, 51, 53], task scheduling [12, 14, 16, 29], processor resource allocation [49], and many others [36, 37]. In this work, we employ machine learning techniques to develop an automatic and portable approach to characterize the scalability of SpMV on an emerging many-core architecture. We stress that this work does not seek to advance machine learning algorithms; instead, it explores and applies a well-established modeling method to tackle the optimization problem for an important class of applications.

7 Conclusion

This paper has presented an empirical study of SpMV scalability on an emerging ARMv8-based many-core architecture, Phytium FT-2000+. We conduct an overall evaluation about the scalability of SpMV on FT-2000+. We develop a machine learning based model to help find the main factors that lead to the flat scalability: unbalanced nonzero allocation, shared L2 cache contention and nonzero variance per row. We use a statistical method to find the relations between factors and the speedup of SpMV as a verification of our model. We select representative matrices to explain how these factors give a limit to the scalability of SpMV on FT-2000+ in an essential way not remain it in “black box”. Along the line, we give potential optimizations for mitigating these scalability bottlenecks on SpMV. Our experimental results show that our optimization can effectively improve the scalability of specific matrices.

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