Three New Probabilistic Models for Dependency Parsing: An Exploration

Jason M. Eisner
CIS Department, University of Pennsylvania
200 S. 33rd St., Philadelphia, PA 19104-6389, USA
jeisner@linc.cis.upenn.edu

Abstract

After presenting a novel $O(n^3)$ parsing algorithm for dependency grammar, we develop three contrasting ways to stochasticize it. We propose (a) a lexical affinity model where words struggle to modify each other, (b) a sense tagging model where words fluctuate randomly in their selectional preferences, and (c) a generative model where the speaker fleshes out each word’s syntactic and conceptual structure without regard to the implications for the hearer. We also give preliminary empirical results from evaluating the three models’ parsing performance on annotated Wall Street Journal training text (derived from the Penn Treebank). In these results, the generative model performs significantly better than the others, and does about equally well at assigning part-of-speech tags.

1 Introduction

In recent years, the statistical parsing community has begun to reach out for syntactic formalisms that recognize the individuality of words. Link grammars (Sleator and Temperley, 1991) and lexicalized tree-adjoining grammars (Schabes, 1992) have now received stochastic treatments. Other researchers, not wishing to abandon context-free grammar (CFG) but disillusioned with its lexical blind spot, have tried to re-parameterize stochastic CFG in context-sensitive ways (Black et al., 1992) or have augmented the formalism with lexical headwords (Magerman, 1995; Collins, 1996).

In this paper, we present a flexible probabilistic parser that simultaneously assigns both part-of-speech tags and a bare-bones dependency structure (illustrated in Figure 1). The choice of a simple syntactic structure is deliberate: we would like to ask some basic questions about where lexical relationships appear and how best to exploit them. It is useful to look into these basic questions before trying to fine-tune the performance of systems whose behavior is harder to understand.

The main contribution of the work is to propose three distinct, lexicalist hypotheses about the probability space underlying sentence structure. We illustrate how each hypothesis is expressed in a dependency framework, and how each can be used to guide our parser toward its favored solution. Finally, we point to experimental results that compare the three hypotheses’ parsing performance on sentences from the Wall Street Journal. The parser is trained on an annotated corpus; no hand-written grammar is required.

2 Probabilistic Dependencies

It cannot be emphasized too strongly that a grammatical representation (dependency parses, tag sequences, phrase-structure trees) does not entail any particular probability model. In principle, one could model the distribution of dependency parses

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1 Our novel parsing algorithm also rescues dependency from certain criticisms: “Dependency grammars . . . are not lexical, and (as far as we know) lack a parsing algorithm of efficiency comparable to link grammars.” (Lafferty et al., 1992, p. 3)
in any number of sensible or perverse ways. The choice of the right model is not \emph{a priori} obvious.

One way to build a probabilistic grammar is to specify what sequences of moves (such as shift and reduce) a parser is likely to make. It is reasonable to expect a given move to be correct about as often on test data as on training data. This is the philosophy behind stochastic CFG (Jelinek et al. 1992), “history-based” phrase-structure parsing (Black et al., 1992), and others.

However, probability models derived from parsers sometimes focus on incidental properties of the data. This may be the case for (Lafferty et al., 1992)'s model for link grammar. If we were to adapt their top-down stochastic parsing strategy to the rather similar case of dependency grammar, we would find their elementary probabilities tabulating only non-intuitive aspects of the parse structure:

\begin{equation}
Pr(\text{word } j \text{ is the rightmost pre-}k \text{ child of word } i \mid i \text{ is a right-spine strict descendant of one of the left children of a token of word } k, \text{ or else } i \text{ is the parent of } k, \text{ and } i \text{ precedes } j \text{ precedes } k) \tag{2}
\end{equation}

While it is clearly necessary to decide whether \( j \) is a child of \( i \), conditioning that decision as above may not reduce its test entropy as much as a more linguistically perspicuous condition would.

We believe it is fruitful to design probability models independently of the parser. In this section, we will outline the three lexicalist, linguistically perspicuous, qualitatively different models that we have developed and tested.

2.1 Model A: Bigram lexical affinities

\( N \)-gram taggers like (Church, 1988; Jelinek 1985; Kupiec 1992; Merialdo 1990) take the following view of how a tagged sentence enters the world. First, a sequence of tags is generated according to a Markov process, with the random choice of each tag conditioned on the previous two tags. Second, a word is chosen conditional on each tag.

Since our sentences have links as well as tags and words, suppose that after the words are inserted, each sentence passes through a third step that looks at each pair of words and randomly decides whether to link them. For the resulting sentences to resemble real corpora, the probability that word \( j \) gets linked to word \( i \) should be \emph{lexically sensitive}; it should depend on the \texttt{(tag,word)} pairs at both \( i \) and \( j \).

The probability of drawing a given parsed sentence from the population may then be expressed as \( \frac{1}{2} \) in Figure 3, where the random variable \( L_{ij} \in \{0, 1\} \) is 1 iff word \( i \) is the parent of word \( j \).

Expression \( \frac{1}{2} \) assigns a probability to every possible tag and link-annotated string, and these probabilities sum to one. Many of the annotated strings exhibit violations such as crossing links and multiple parents—which, if they were allowed, would let all the words express their lexical preferences independently and simultaneously. We stipulate that the model discards from the population any illegal structures that it generates; they do not appear in either training or test data. Therefore, the parser described below finds the likeliest \emph{legal} structure: it maximizes the lexical preferences of \( \frac{1}{2} \) within the few hard linguistic \emph{constraints} imposed by the dependency formalism.

In practice, some generalization or “coarsening” of the conditional probabilities in \( \frac{1}{2} \) helps to avoid the effects of undertraining. For example, we follow standard practice (Church, 1988) in \( n \)-gram tagging by using \( \frac{1}{2} \) to approximate the first term in \( \frac{1}{2} \). Decisions about how much coarsening to do are of great practical interest, but they depend on the training corpus and may be omitted from a conceptual discussion of the model.

The model in \( \frac{1}{2} \) can be improved; it does not capture the fact that words have arities. For example, the \textit{price of the stock fell} (Figure 3a) will typically be misanalyzed under this model. Since stocks often fall, \textit{stock} has a greater affinity for \textit{fell} than for \textit{of}. Hence \textit{stock} (as well as \textit{price}) will end up pointing to the verb \textit{fell} (Figure 3b), resulting in a double subject for \textit{fell} and leaving \textit{of} childless.

To capture word arities and other subcategorization facts, we must recognize that the children of a word like \textit{fell} are not independent of each other.

The solution is to modify \( \frac{1}{2} \) slightly, further conditioning \( L_{ij} \) on the number and/or type of children of \( i \) that already sit between \( i \) and \( j \). This means that in the parse of Figure 3a, the link \textit{price} \( \rightarrow \textit{fell} \) will be sensitive to the fact that \textit{fell} already has a closer child tagged as a noun (NN). Specifically, the \textit{price} \( \rightarrow \textit{fell} \) link will now be strongly disfavored in Figure 3a, since verbs rarely take two NN dependents to the left. By contrast, \textit{price} \( \rightarrow \textit{fell} \) is unobjectionable in Figure 3b, since verbs rarely take two NN dependents to the left. In any legal dependency parse, every word except for the head of the sentence (the EOS mark) has
\[ Pr(\text{words, tags, links}) = Pr(\text{words, tags}) \cdot Pr(\text{link presences and absences | words, tags}) \]
\[ \approx \prod_{1 \leq i \leq n} Pr(tword(i) | tword(i+1), tword(i+2)) \cdot \prod_{1 \leq i,j \leq n} Pr(L_{ij} | tword(i), tword(j)) \]
\[ Pr(tword(i) | tword(i+1), tword(i+2)) \approx Pr(\text{tag}(i) | \text{tag}(i+1), \text{tag}(i+2)) \cdot Pr(\text{word}(i) | \text{tag}(i)) \]
\[ Pr(\text{words, tags, links}) \propto Pr(\text{words, tags, preferences}) = Pr(\text{words, tags}) \cdot Pr(\text{preferences | words, tags}) \]
\[ \approx \prod_{1 \leq i \leq n} Pr(tword(i) | tword(i+1), tword(i+2)) \cdot \prod_{1 \leq i \leq n} Pr(\text{preferences}(i) | tword(i)) \]
\[ Pr(\text{words, tags, links}) = \prod_{1 \leq i \leq n} \left( \prod_{1 \leq j \leq n} Pr(tword(\text{kid}_j(i)) | \text{tag}(\text{kid}_{j-1}(i)), tword(i)) \right) \]

Figure 2: High-level views of model A (formulas 1–3); model B (formula 4); and model C (formula 5). If \( i \) and \( j \) are tokens, then \( tword(i) \) represents the pair \( \langle \text{tag}(i), \text{word}(i) \rangle \), and \( L_{ij} \in \{0,1\} \) is 1 iff \( i \) is the parent of \( j \).

exactly one parent. Rather than having the model select a subset of the \( n^2 \) possible links, as in model A, and then discard the result unless each word has exactly one parent, we might restrict the model to picking out one parent per word to begin with. Model B generates a sequence of tagged words, then specifies a parent—or more precisely, a type of parent—for each word \( j \).

Of course model A also ends up selecting a parent for each word, but its calculation plays careful politics with the set of other words that happen to appear in the sentence: word \( j \) considers both the benefit of selecting \( i \) as a parent, and the costs of spurning all the other possible parents \( i \). Model B takes an approach at the opposite extreme, and simply has each word blindly describe its ideal parent. For example, \textit{price} in Figure 2 might insist (with some probability) that it “depend on a verb to my right.” To capture arity, words probabilistically specify their ideal children as well: \textit{fell} is highly likely to want only one noun to its left. The form and coarseness of such specifications is a parameter of the model.

When a word stochastically chooses one set of requirements on its parents and children, it is choosing what a link grammarian would call a disjunct (set of selectional preferences) for the word. We may thus imagine generating a Markov sequence of tagged words as before, and then independently “sense tagging” each word with a disjunct. Choosing all the disjuncts does not quite specify a parse. However, if the disjuncts are sufficiently specific, it specifies at most one parse. Some sentences generated in this way are illegal because their disjuncts cannot be simultaneously satisfied; as in model A, these sentences are said to be removed from the population, and the probabilities renormalized. A likely parse is therefore one that allows a likely and consistent set of sense tags; its probability in the population is given in (4).

2.3 Model C: Recursive generation

The final model we propose is a generation model, as opposed to the comprehension models A and B (and to other comprehension models such as (Lafferty et al., 1992; Magerman, 1995; Collins, 1996)). The contrast recalls an old debate over spoken language, as to whether its properties are driven by hearers’ acoustic needs (comprehension) or speakers’ articulatory needs (generation). Models A and B suggest that speakers produce text in such a way that the grammatical relations can be easily decoded by a listener, given words’ preferences to associate with each other and tags’ preferences to follow each other. But model C says that speakers’ primary goal is to flesh out the syntactic and conceptual structure for each word they utter, surrounding it with arguments, modifiers, and function words as appropriate. According to model C, speakers should not hesitate to add extra prepositional phrases to a noun, even if this lengthens some links that are ordinarily short, or leads to tagging or attachment ambiguities.

The generation process is straightforward. Each time a word \( i \) is added, it generates a Markov sequence of (tag,word) pairs to serve as its left children, and an separate sequence of (tag,word) pairs as its right children. Each Markov process, whose probabilities depend on the word \( i \) and its tag, begins in a special START state; the symbols it generates are added as \( i \)'s children, from closest to farthest, until it reaches the STOP state. The process recurses for each child so generated. This is a sort of lexicalized context-free model.

Suppose that the Markov process, when generating a child, remembers just the tag of the child’s most recently generated sister, if any. Then the probability of drawing a given parse from the population is (5), where \( \text{kid}(i,c) \) denotes the \( c \)-closest right child of word \( i \), and where \( \text{kid}(i,0) = \text{START} \) and \( \text{kid}(i,1 + \#\text{right-kids}(i)) = \text{STOP} \).
Figure 4: Spans participating in the correct parse of That dachshund over there can really play golf!. (a) has one parentless endword; its subspan (b) has two.

(c < 0 indexes left children.) This may be thought of as a non-linear trigram model, where each tagged word is generated based on the parent tagged word and a sister tag. The links in the parse serve to pick out the relevant trigrams, and are chosen to get trigrams that optimize the global tagging. That the links also happen to annotate useful semantic relations is, from this perspective, quite accidental.

Note that the revised version of model A uses probabilities \( P_r(\text{link to child} \mid \text{child, parent, closer-children}) \), where model C uses \( P_r(\text{link to child} \mid \text{parent, closer-children}) \). This is because model A assumes that the child was previously generated by a linear process, and all that is necessary is to link to it. Model C actually generates the child in the process of linking to it.

3 Bottom-Up Dependency Parsing

In this section we sketch our dependency parsing algorithm: a novel dynamic-programming method to assemble the most probable parse from the bottom up. The algorithm adds one link at a time, making it easy to multiply out the models’ probability factors. It also enforces the special directionality requirements of dependency grammar: the prohibitions on cycles and multiple parents.

The method used is similar to the CKY method of context-free parsing, which combines analyses of shorter substrings into analyses of progressively longer ones. Multiple analyses have the same signature if they are indistinguishable in their ability to combine with other analyses; if so, the parser discards all but the highest-scoring one. CKY requires \( O(n^3s^2) \) time and \( O(n^2s) \) space, where \( n \) is the length of the sentence and \( s \) is an upper bound on signatures per substring.

Let us consider dependency parsing in this framework. One might guess that each substring analysis should be a lexical tree—a tagged headword plus all lexical subtrees dependent upon it. (See Figure 5b.) However, if a constituent’s probabilistic behavior depends on its headword—the lexicalist hypothesis—then differently headed analyses need different signatures. There are at least \( k \) of these for a substring of length \( k \), whence the bound \( s = k = \Omega(n) \), giving a time complexity of \( \Omega(n^5) \). (Collins, 1996) uses this \( \Omega(n^5) \) algorithm directly (together with pruning).

We propose an alternative approach that preserves the \( O(n^3) \) bound. Instead of analyzing substrings as lexical trees that will be linked together into larger lexical trees, the parser will analyze them as non-constituent spans that will be concatenated into larger spans. A span consists of \( \geq 2 \) adjacent words; tags for all these words except possibly the last; a list of all dependency links among the words in the span; and perhaps some other information carried along in the span’s signature. No cycles, multiple parents, or crossing links are allowed in the span, and each internal word of the span must have a parent in the span.

Two spans are illustrated in Figure 4. These diagrams are typical: a span of a dependency parse may consist of either a parentless endword and some of its descendants on one side (Figure 4a), or two parentless endwords, with all the right descendants of one and all the left descendants of the other (Figure 4b). The intuition is that the internal part of a span is grammatically inert: except for the endwords dachshund and play, the structure of each span is irrelevant to the span’s ability to combine in future, so spans with different internal structure can compete to be the best-scoring span with a particular signature.

If span \( a \) ends on the same word \( i \) that starts span \( b \), then the parser tries to combine the two spans by covered-concatenation (Figure 5). The two copies of word \( i \) are identified, after which a leftward or rightward covering link is optionally added between the endwords of the new span. Any dependency parse can be built up by covered-concatenation. When the parser covered-concatenates \( a \) and \( b \), it obtains up to three new spans (leftward, rightward, and no covering link).

The covered-concatenation of \( a \) and \( b \), forming \( c \), is barred unless it meets certain simple tests:

- \( a \) must be minimal (not itself expressible as a concatenation of narrower spans).
- Since the overlapping word will be internal to \( c \), it must have a parent in exactly one of \( a \) and \( b \).
The third factor depends on, e.g., $\text{kid}(i, c - 1)$, which we recover from the span signature. Also, matters are complicated slightly by the probabilities associated with the generation of STOP.

\footnote{Different $k - \ell$ spans have scores conditioned on different hypotheses about $\text{tag}(\ell)$ and $\text{tag}(\ell + 1)$; their signatures are correspondingly different. Under model B, a $k - \ell$ span may not combine with an $\ell - m$ span whose tags violate its assumptions about $\ell$ and $\ell + 1$.}

Different $k - \ell$ spans have scores conditioned on different hypotheses about $\text{tag}(\ell)$ and $\text{tag}(\ell + 1)$; their signatures are correspondingly different. Under model B, a $k - \ell$ span may not combine with an $\ell - m$ span whose tags violate its assumptions about $\ell$ and $\ell + 1$. 

|        | A (%) | B (%) | C (%) | X (%) | Baseline (%) |
|--------|-------|-------|-------|-------|--------------|
| All tokn | 90.2  | 90.9  | 90.8  | 90.5  | 91.0         |
| Nouns   | 88.9  | 89.8  | 89.8  | 89.3  | 90.2         |
| Lex verbs | 74.6  | 75.9  | 73.3  | 75.8  | 73.3         | 67.5

Table 1: Results of preliminary experiments: Percentage of tokens correctly tagged by each model.

which is replaced by the less obvious expression in (6) as noted above. As usual, scores can be constructed from the bottom up (though $\text{tword}(j)$ in the second factor of (6) is not available to the algorithm, $j$ being outside the span, so we back off to $\text{tword}(j)$).

5 Empirical Comparison

We have undertaken a careful study to compare these models’ success at generalizing from training data to test data. Full results on a moderate corpus of 25,000+ tagged, dependency-annotated Wall Street Journal sentences, discussed in (Eisner, 1996), were not complete at press time. However, Tables 1-2 show pilot results for a small set of data drawn from that corpus. (The full results show substantially better performance, e.g., 93% correct tags and 87% correct parents for model C, but appear qualitatively similar.)

The pilot experiment was conducted on a subset of 4772 of the sentences comprising 93,360 words and punctuation marks. The corpus was derived by semi-automatic means from the Penn Treebank; only sentences without conjunction were available (mean length=20, max=68). A randomly selected set of 400 sentences was set aside for testing all models; the rest were used to estimate the model parameters. In the pilot (unlike the full experiment), the parser was instructed to “back off” from all probabilities with denominators < 10. For this reason, the models were insensitive to most lexical distinctions.

In addition to models A, B, and C, described above, the pilot experiment evaluated two other models for comparison. Model C’ was a version of model C that ignored lexical dependencies between parents and children, considering only dependencies between a parent’s tag and a child’s tag. This model is similar to the model used by stochastic CFG. Model X did the same n-gram tagging as models A and B ($n = 2$ for the preliminary experiment, rather than $n = 3$), but did not assign any links.

Tables 1-2 show the percentage of raw tokens that were correctly tagged by each model, as well as the proportion that were correctly attached to
Table 2: Results of preliminary experiments: Percentage of tokens correctly attached to their parents by each model.

|          | A (%) | B (%) | C (%) | C' (%) | Baseline (A) |
|----------|-------|-------|-------|-------|--------------|
| All tokens | 74.9  | 72.5  | 70.1  | 69.9  | 72.2         |
| Non-punc  | 75.0  | 75.4  | 70.2  | 68.8  | 51.1         |
| Nouns     | 75.7  | 71.8  | 77.2  | 55.9  | 29.8         |
| Lexical verbs | 66.5 | 63.1  | 71.0  | 46.9  | 21.0         |

As a first step in the study of lexical affinity, we asked whether there was a “natural” way to stochasticize such a simple formalism as dependency. In fact, we have now exhibited three promising types of models for this simple problem. Further, we have developed a novel parsing algorithm to compare these hypotheses, with results that so far favor the speaker-oriented model C, even in written, edited Wall Street Journal text. To our knowledge, the relative merits of speaker-oriented versus hearer-oriented probabilistic syntax models have not been investigated before.

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6 Conclusions

Bare-bones dependency grammar—which requires no link labels, no grammar, and no fuss to understand—is a clean testbed for studying the lexical affinities of words. We believe that this is an important line of investigative research, one that is likely to produce both useful parsing tools and significant insights about language modeling.

7 We used distinctive tags for auxiliary verbs and for words being used as noun modifiers (e.g., participles), because they have very different subcategorization frames.