Virtual Citation Proximity (VCP): Empowering Document Recommender Systems by Learning a Hypothetical In-Text Citation-Proximity Metric for Uncited Documents

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Abstract
The relatedness of research articles, patents, court rulings, web pages, and other document types is often calculated with citation or hyperlink-based approaches like co-citation (proximity) analysis. The main limitation of citation-based approaches is that they cannot be used for documents that receive little or no citations. We propose Virtual Citation Proximity (VCP), a Siamese Neural Network architecture, which combines the advantages of co-citation proximity analysis (diverse notions of relatedness / high recommendation performance), with the advantage of content-based filtering (high coverage). VCP is trained on a corpus of documents with textual features, and with real citation proximity as ground truth. VCP then predicts for any two documents, based on their title and abstract, in what proximity the two documents would be co-cited, if they were indeed co-cited. The prediction can be used in the same way as real citation proximity to calculate document relatedness, even for uncited documents. In our evaluation with 2 million co-citations from Wikipedia articles, VCP achieves an MAE of 0.0055, i.e. an improvement of 20% over the baseline, though the learning curve suggests that more work is needed.

1 Introduction
Calculating document relatedness is key in creating recommender systems for digital libraries (we focus on research paper recommenders – our work is, however, equally applicable to patents, websites, court rulings and other documents with hyperlinks, citations respectively). Recommender systems in digital libraries calculate relatedness of research articles typically via content-based filtering or hyperlink/citation-based approaches (Jannach et al., 2010; Beel et al., 2016; Lops et al., 2019). Citation-based approaches consider documents as related that reference the same documents (bibliographic coupling), that are co-cited by other documents or that are otherwise connected in the citation graph (Beel et al., 2016).

Citation-based approaches may recommend more diverse items than content-based filtering, as citations can be made for various reasons (Willett, 2013; Färber and Sampath, 2019; Erikson and Erlandson, 2014). For instance, two documents can be co-cited because they address the same research problem; use the same methodology (to solve different problems); or two documents may be co-cited for less predictable reasons. Today’s text-based methods can hardly distinguish such diverse types of relatedness. Instead, text-based methods generally consider two documents as related the more terms they have in common.

A particularly promising citation-based approach is Citation Proximity Analysis (CPA) (Gipp and Beel, 2009), which is illustrated in Figure 1. CPA considers documents as the more related, the closer the distance in which they are co-cited. CPA out-performs standard co-citation analysis by up to 95% (Schwarzer et al., 2016) and has successfully been used with research articles (Balaji et al., 2017; Liu and Chen, 2011; Knoth and Khadka, 2017; Gipp and Beel, 2009), Wikipedia (Schwarzer et al., 2016, 2017), web pages (Gipp et al., 2010), mind-maps (Beel and Gipp, 2010) and authors (Kim et al., 2016). The downside of CPA is that it can be only be applied to documents that are (co-)cited. Most research articles, however, are

1Of course, there are multiple approaches like word embeddings that go beyond a simple term-overlap comparison. However, eventually, text-based approaches focus on content similarity, which is just one type of relatedness.
A citing document cites the three documents A, B, and C. Documents A and B are cited within the same sentence and are hence strongly related. Documents A and C, as well as documents B and C, are each cited within different paragraphs. Hence, they are considered as less strongly related to each other. A recommender system that receives document B as input, and that should recommend the most related document, would recommend document A.

never cited, and even if they are, it usually takes a year or more before they receive their first citation (Golosovsky, 2017; Abramo et al., 2016). Consequently, CPA has a low coverage, i.e. it can only be applied to a small fraction of research articles in a corpus and only relatively late.

We propose\(^2\), implement and evaluate a novel approach that we name ’Virtual Citation Proximity’ (VCP). We hypothesize that VCP combines the advantages of co-citation proximity analysis (diverse notions of relatedness / high recommendation effectiveness), with the advantage of content-based filtering (high coverage). Hence, we expect that VCP advances the state-of-the-art in related-document calculations for search engines and recommender systems significantly.

### 2 Virtual Citation Proximity (VCP)

Virtual Citation Proximity (VCP) predicts in which distance two documents – that are not co-cited – would be co-cited if they were co-cited. This predicted proximity can then be used in the same way as real co-citation proximity to calculate document relatedness. At an abstract level, the idea behind VCP is that there is an inherent concept of relatedness between articles. This inherent relatedness can be described either through text or co-citations. As both, text and citations, eventually refer to the same relatedness, the text and citation are kind of a ‘siamese twin’.

We propose to implement VCP via artificial neural networks that are trained with textual features – e.g. terms or word embeddings from the title or abstract – as input, and real citation proximity as target. In other words, we feed a neural network with pairs of documents of which we know how strongly they are related (expressed by the real proximity of their co-citations). The network then learns a similarity function that predicts based on the text the degree to which the two documents are related – even if the two documents have no terms or word embeddings in common.

We hypothesize that a neural network will be able to learn the diverse types of relatedness inherent to co-citations. Once the network is trained, it receives the text of two documents as input, and predicts in what proximity these two documents would be co-cited if they were co-cited. VCP can be applied to all document pairs in a corpus that contain a title (and abstract), i.e. typically all document in a corpus (100% coverage). If the predictions of VCP are precise, a recommender system based on VCP would be as effective as a system based on real citation proximity, but with a coverage as high as content-based filtering (100%).

Although Virtual Citation Proximity is based on textual features as input, we hypothesise that VCP will create recommendations similar to those based on real citation-proximity, since the machine learning algorithm is trained on real citation proximity as ground truth. With the recent advances in (deep) machine learning we hypothesise that a (deep) machine-learning algorithm will be able to detect hidden layers in the text. These will allow determining what makes two documents related, more reliable than the typical assumption in text-based approaches that two documents are related when they share the same terms or embeddings.

### 3 Related Work

Virtual Citation Proximity trains a machine learning model with real citation proximity as ground
truth / target, and to the best of our knowledge we are first to do this. The method that is closest to using citation-proximity as ground truth for machine learning is using expert judgements (or knowledge bases) as ground truth, e.g. MeSH, ACM CCS, or DMOZ (Mohammadi et al., 2016; Hassan, 2017).

For instance, the MeSH classification is a classification tree that represents the major fields and sub-fields in the biomedical domain. MeSH was created by medical experts and biomedical manuscripts are often classified with MeSH, i.e. manuscripts are assigned to one of the MeSH categories, whereas two documents in the same category are considered to be related, and can be used either for training machine learning models or evaluating recommendation approaches (Hassan, 2017). Machine learning algorithms can infer from the existing documents in a category, which textual features make a document likely to belong to a certain category. New documents can then automatically be classified based on their text (Peng et al., 2018).

There are disadvantages to using expert classifications like MeSH, when compared to citations and VCP respectively. First, expert classifications are often one-dimensional, i.e. they provide only one type of relatedness (typically, the overall topic a research article is about). Second, most expert classification schemes allow documents to be in few categories only, and they focus on one field (e.g. medicine or computer science). Especially with today’s increasingly interdisciplinary work, this is often not enough to adequately find all related documents. Third, classification schemes typically have a limited number of categories (a few thousand at most). This means, in large collections, categories contain thousands of documents that are somewhat related to each other but only at a relatively broad level. Fourth, classifications are often static, i.e. articles are classified at the time of publication. If a classification scheme is changed, the papers are not updated or re-classified. Finally, for many domains, expert classifications simply do not exist.

With VCP, the problems could be overcome. (Virtual) citation proximity (1) covers many types of relatedness; (2) allows documents to be in unlimited numbers of co-citation clusters; (3) has no limitations for the number of clusters; (4) is dynamic; and (5) can be learned for any domain that uses citations.

In recent years advances in deep-learning have shown the ability to identify complex patterns in text based data in areas such as translation (Wu et al., 2016) and sentiment analysis (Dos Santos and Gatti, 2014).

A document embedding (Le and Mikolov, 2014; Dai et al., 2015) is an embedding representing an entire document trained using a paragraph embedding model. Document embedding vectors have been shown to be superior to other text representations such as bag-of-words as they take into account the relative positions of the words in the text, although experimental they may be an interesting feature representation to train VCP. Overall, papers with success in using machine learning for dealing with larger passages of text more limited in number (Liu et al., 2018), compared to longer texts (Lopez and Kalita, 2017). Some relevant research was found in the areas of news article recommender systems (Park et al., 2017).

4 Methodology

4.1 VCP Implementation

We implement four VCP variations. The first implementation is a sequential neural network with a CNN and LSTM layer with drop-out. The second, third and fourth implementation are Siamese neural networks, whereas the second implementation consists of two LSTM layers with drop-out (Figure 3); the third implementation consists of a CNN and LSTM layer with drop-out; and the fourth implementation consists of a CNN and LSTM layer with no drop-out. The Siamese architectures finish with a sequential dense layer to join the sub-networks. We choose combinations of 200-neuron
LSTM and 64-filter CNN layers in both sequential and Siamese architectures.

So far, Siamese networks have been particularly successful in face recognition. During training, the network receives a triplet as input consisting of an anchor image of a person A, another image of the same person, and an image of a person that is not A. The network is trained to learn a similarity or distance function that can express the high similarity (or low distance) of the anchor image and images of the same person, and dissimilarity (or high distance) of the anchor image and negative person. Siamese networks also have been successfully used to learn text similarity (Mueller and Thyagarajan, 2016). Siamese architectures facilitate the sister sub-networks to learn high level representations from both input texts first. Then once the Siamese Neural Network has transformed the input into higher level representations they can be combined together again to determine the relationship between the two texts.

In our scenario, triplets consist of an anchor citation and a close co-citation (as both express the same semantic concept) as well as of a document that is dissimilar to the anchor citation. We hypothesize that a neural network that is capable of learning the abstract concept of a "person", based on vastly different images (pixels) of that person, should also be able to learn the abstract semantic concept of relatedness, based on vastly different documents (textual features) and citation proximity.

Each of the four implementations takes as input two documents represented by their title and the first 200 words of the body text, and predicts the distance in which these two documents would be co-cited, if they were co-cited. All VCP variations used the GloVe6B word embedding model to represent textual features. We used Glove6B out-of-box, i.e. trained on a dump from English Wikipedia in 2014, and with 100 dimensions. All four models were implemented in Keras, and trained over 50 epochs. The source code and data is available on GitHub https://github.com/BeelGroup/Virtual-Citation-Proximity/.

We need to emphasize that we did not compare our implementations against a state-of-the-art baseline as there does not exist any other work that predicts citation proximity. Hence, we only compare the performance of our models against a trivial baseline, i.e. the average co-citation proximity in the corpus. In the future, the predicted citation proximity should be used in a recommender system and could then be compared against baselines like content-based filtering.

4.2 Dataset

We initially aimed to use research papers and citations for our experiments. Eventually, we decided to choose Wikipedia as a substitute. Parsing research papers (PDF files) for their in-text citation was too computationally expensive and error prone, and we did not find existing suitable dataset that would have contained enough in-text citation data. Wikipedia contains millions of articles, that are somewhat comparable to research articles, and these articles contain hyperlinks, that are comparable to citations. Also, Wikipedia data is machine readable, i.e. hyperlinks/citations can easily be identified. We used the Wikipedia dump from January 1st 2019 with 15 million articles, of which we choose a random sample (filtering out articles co-cited less than 5 times) of 1,000 articles and all articles co-cited with those sample articles. This resulted in 2.1 million co-citation pairs.

A key factor in citation proximity analysis is the question how to exactly measure proximity, or distance. The original authors of Citation Proximity Analysis expressed the distance between two co-citations through a 'citation proximity index' (CPI) (Gipp and Beel, 2009). If two documents were co-cited in the same sentence, CPI was 1; if documents were co-cited in the same paragraph, CPI was 0.5; and so on (Table 1). Many more variations have been proposed, such as the use of machine learning to predict citation proximity.

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3unarXive (Saier and Färber, 2020) might be suitable, but it was just released after we conducted our experiments.
been proposed to calculate CPIs, e.g. (Kim et al., 2016). We follow Schwarzer et al. including their suggested damping factor \( \alpha \) of 0.855 to scale word distance (Schwarzer et al., 2016).

\[
CPI(a, b) = \sum_{j=1}^{m} \Delta_j(a, b)^{-\alpha},
\]

with \( \Delta_j(a, b)^{-\alpha} = \left\{ \begin{array}{ll}
|v_{a,j} - v_{b,j}|^{-\alpha}, & v_{a,j} > 0 \land v_{b,j} > 0 \\
0, & \text{otherwise}
\end{array} \right. \) (1)

Table 1: CPI values for co-cited document pairs, as proposed by the original authors (Gipp and Beel, 2009). However, these values are only for a single occurrence of a co-citation pair. If, e.g., documents A and B are co-cited by document C in the same sentence but by document D in different paragraphs, the final CPI value must be a fusion of these CPI values (e.g. the min, max or average).

| Occurrence                        | CPI Value |
|-----------------------------------|-----------|
| Sentence                          | 1         |
| Paragraph                         | 1/2       |
| Chapter                           | 1/4       |
| Same journal / same book          | 1/8       |
| Same journal but different edition| 1/16      |

A second important question is how to deal with multiple occurrences of the same co-citation pair in different documents, and hence different CPI values for each occurrence. The most simple solutions are using the minimum, average or sum of the individual CPIs (Knoth and Khadka, 2017). We choose for our work the average CPI as this has been shown to be among the most effective choices typically (Knoth and Khadka, 2017). We calculated CPI values with the tool Citolytics (Schwarzer et al., 2017)4 as per the equation below, based on Schwarzer et al.. \((a, b)\) is a document pair with \( m \) co-citations and \( v_{a,j} \) is the position in words of the \( j \)th citation of \( a \). See example data (Table 2).

4.3 Evaluation Metric

We evaluate the VCP implementations based on how well they predict the actual CPI, which theoretically takes values between 0 and 1, but typically is between 0 and 0.1 (Figure 4). Performance is measured by mean absolute error (MAE).

We have not yet conducted additional recommender-system specific experiments. We assume that the more precise the prediction of the CPIs are, the better the recommendation performance becomes. Of course, this is a strong assumption that needs to be validated in future experiments.

5 Results and Discussion

All four models achieved relatively low MAEs between 0.0059 (Sequential 1D CNN + LSTM) and 0.0055 (Siamese LSTM + LSTM; Siamese CNN + LSTM, No Dropout) (Figure 5). All three Siamese Neural Networks outperformed the simple Sequential model CNN+LSTM. The differences among the three Siamese architectures are statistically not significant. All four models performed statistically significant better (\( p < 0.01; \) two-tailed t-test) than the baseline, i.e. the mean CPI in the dataset (MAE=0.0069). The low MAEs must be seen with some skepticism. The average of the actual CPI values in the dataset was 0.0069 with data skewed towards smaller values. Hence, an MAE of e.g. 0.0055 is promising (20% lower, i.e. better, than...
Table 2: Citolytics Wikipedia CPI Pair Dataset Format Example.

| Hash | Title A | Title B | Dist | Count | Title A ID | Title B ID | CPI  |
|------|---------|---------|------|-------|------------|------------|------|
| -124 | USA     | USSR    | 312  | 12    | 5          | 7          | 0.26 |

The learning curves of the four VCP approaches indicate that citation proximity could not be learned very effectively. Figure 6 shows the training and validation error rates of the Siamese CNN + LSTM Model over 50 epochs. The validation error shows that no real learning occurs after the first epoch.

Overall, our result, i.e. a 20% improvement over the trivial ‘mean’ baseline, is promising but more research is needed to confirm the effectiveness of Virtual Citation Proximity. In the current experiment, we used the average CPI of document pairs as target, but alternatives such as the minimum or maximum CPI might be easier to learn for a Siamese network. Also, there were many documents with low CPI values in the corpus, which might have introduced noise. In future work, we would focus on documents with higher CPI values as we expect their signal to be stronger. We also plan to use more than 200 words in future experiments, as more words might contain more semantic meaning of why a document was cited. Maybe most importantly, Virtual Citation Proximity needs to be evaluated in more recommender-system specific experiments. So far, we ‘only’ predicted citation distance. The key question, however, is how good

VCP-based recommendations can be, i.e. how precise they need to be to contribute to business value (Jannach and Jugovac, 2019). It will also be interesting to see how VCP compares with content-based filtering, citation-based approaches, and machine learning models trained on expert opinions as ground truth.

While our initial results are ‘only’ good, we see an enormous potential in Virtual Citation Proximity for improving recommender systems for research papers, web pages, patents, and other document types. We are confident that VCP could become
a new state-of-the-art approach for research paper recommender systems that brings citation-based recommendation effectiveness to the community, applicable to all textual documents. In the best case, VCP might even outperform citation based approaches as VCP learns from both terms and citations and hence VCP might be able to learn semantic concepts in a completely new way beyond traditional citation and content analysis.

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