Dilepton radiation by vector mesons and off-shell partons in the hot and dense medium

O. Linnyka, E. L. Bratkovskayaa and W. Cassingb

aInstitut für Theoretische Physik, Universität Frankfurt, 60438 Frankfurt am Main, Germany
bInstitut für Theoretische Physik, Universität Giessen, 35392 Giessen, Germany

According to the dynamical quasiparticle model (DQPM) – matched to reproduce lattice QCD results in thermodynamic limit – the constituents of the strongly interacting quark-gluon plasma (sQGP) are massive and off-shell quasi-particles (quarks and gluons) with broad spectral functions. In order to address the electromagnetic radiation of the sQGP, we derive off-shell cross sections of \( q\bar{q} \rightarrow \gamma^* \), \( q\bar{q} \rightarrow \gamma^* + g \) and \( gg \rightarrow \gamma^* q(qg \rightarrow \gamma^* q) \) reactions taking into account the effective propagators for quarks and gluons from the DQPM. Dilepton production in In+In collisions at 158 AGeV is studied by implementing these processes into the parton-hadron-string dynamics (PHSD) transport approach. The microscopic PHSD transport approach describes the full evolution of the heavy-ion collision: from the dynamics of quasi-particles in the sQGP phase (when the local energy density is above \( \sim 1 \text{ GeV/fm}^3 \)) through hadronization and to the following hadron interactions and off-shell propagation after the hadronization. A comparison to the data of the NA60 Collaboration shows that the low mass dilepton spectra are well described by including a collisional broadening of vector mesons, while the spectra in the intermediate mass range are dominated by off-shell quark-antiquark annihilation, quark Bremsstrahlung and gluon-Compton scattering in the nonperturbative QGP. In particular, the observed softening of the \( m_T \) spectra at intermediate masses (\( 1 \text{ GeV} \leq M \leq 3 \text{ GeV} \)) is approximately reproduced.

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I. INTRODUCTION

While the properties of hadrons are rather well known in free space (embedded in a nonperturbative QCD vacuum) the masses and lifetimes of hadrons in a baryonic and/or mesonic environment are subject of current research in order to achieve a better understanding of the strong interaction and the nature of confinement. A modification of vector mesons has been seen experimentally in the enhanced production of lepton pairs above known sources in nucleus-nucleus collisions at Super-Proton-Synchrotron (SPS) energies [1, 2]. This can be attributed to a shortening of the lifetime of the vector mesons \( \rho, \omega \) and \( \phi \). The question arises if the enhancement might (in part) be due to new radiative channels [3] from the strong Quark-Gluon Plasma (sQGP). The answer to this question is nontrivial due to the nonequilibrium nature of the heavy-ion reactions and covariant transport models have to be incorporated to disentangle the various sources that contribute to the final dilepton spectra seen experimentally.

II. THE PHSD APPROACH

To address the vector meson properties in a hot and dense medium – as created in heavy-ion collisions – we employ an up-to-date relativistic transport model, i.e. the Parton Hadron String Dynamics (PHSD) that incorporates the relevant off-shell dynamics of the vector mesons as well as the explicit partonic phase in the early hot and dense reaction region. PHSD consistently describes the full evolution of a relativistic heavy-ion collision from the initial hard scatterings and string formation through the dynamical deconfinement phase transition to the quark-gluon plasma (QGP) as well as hadronization and to the subsequent interactions in the hadronic phase.

In the hadronic sector PHSD is equivalent to the Hadron-String-Dynamics (HSD) transport approach [4–7] that has been used for the description of \( pA \) and \( AA \) collisions from SIS to RHIC energies and has lead to a fair reproduction of hadron abundances, rapidity distributions and transverse momentum spectra. In particular, HSD incorporates off-shell dynamics for vector mesons – according to Refs. [8] – and a set of vector-meson spectral functions [10] that covers possible scenarios for their in-medium modification. The transport theoretical description of quarks and gluons in PHSD is based on a dynamical quasiparticle model for partons matched to reproduce lattice QCD results in thermodynamic equilibrium (DQPM). The transition from partonic to hadronic degrees of freedom is described by covariant transition rates for the fusion of quark-antiquark pairs to mesonic resonances or three quarks (antiquarks) to baryonic states.

Various models predict that hadrons change in the (hot and dense) nuclear medium; in particular, a broadening of the spectral function or a mass shift of the vector mesons has been expected. Furthermore, QCD sum rules
indicated that a mass shift may lead to a broadening and vice versa [9]; therefore both modifications should be studied simultaneously. Thus we explore three possible scenarios: (1) a broadening of the $\rho$ spectral function, (2) a mass shift, and (3) a broadening plus a mass shift. The HSD (PHSD) off-shell transport approach allows to investigate in a consistent way the different scenarios for the modification of vector mesons in a hot and dense medium. In the off-shell transport, hadron spectral functions change dynamically during the propagation through the medium and evolve towards the on-shell spectral function in the vacuum.

As demonstrated in Ref. [10] the off-shell dynamics is particularly important for resonances with a rather long lifetime in vacuum but strongly decreasing lifetime in the nuclear medium (especially $\omega$ and $\phi$ mesons) but also proves vital for the correct description of dilepton decays of $\rho$ mesons with masses close to the two pion decay threshold. For a detailed description of the various hadronic channels included for dilepton production as well as the off-shell dynamics we refer the reader to Refs. [10, 11].

III. DILEPTON RADIATION FROM THE QUARK GLUON PLASMA

By employing the HSD approach to the low mass dilepton production in relativistic heavy-ion collisions, it was shown in [11] that the NA60 Collaboration data for the invariant mass spectra for $\mu^+\mu^-$ pairs from In+In collisions at 158 A-GeV favored the 'melting $\rho$' scenario [14]. Also the data from the CERES Collaboration [15] showed a preference for the 'melting $\rho$' picture. On the other hand, the dilepton spectrum from In+In collisions at 158 A-GeV for $M > 1$ GeV could not be accounted for by the known hadronic sources (see Fig. 2 of [11]). Also, hadronic models do not reproduce the softening of the $m_T$ distribution of dileptons at $M > 1$ GeV [14]. This observation points towards a partonic origin but needs further examination.

The transport theoretical description of the partonic dynamics in PHSD is based on the Dynamical QuasiParticle Model (DQPM) [13] which describes QCD properties in terms of single-particle Green’s functions (in the sense of a two-particle irreducible approach) and leads to effective strongly interacting partonic quasiparticles with broad spectral functions as degrees of freedom. Dilepton radiation by the constituents of the strongly interacting QGP, i.e. by the dynamical quasiparticles, proceeds via the elementary processes illustrated in Fig. 1 the basic Drell-Yan $q + \bar{q}$ annihilation mechanism, Gluon Compton scattering ($q + g \rightarrow \gamma^* + q$ and $\bar{q} + g \rightarrow \gamma^* + \bar{q}$), and quark + anti-quark annihilation with gluon Bremsstrahlung in the final state ($q + \bar{q} \rightarrow g + \gamma^*$). Note that in our calculations the running coupling $\alpha_S$ depends on the local energy density $\epsilon$ according to the DQPM [13], while the energy density is related to the temperature $T$ by the IQCD equation of state. Numerically, we observe that $\alpha_S$ is of the order $O(1)$ and thus the contribution of the higher order diagrams in Fig. 1 is not subleading!

In the on-shell approximation, one uses perturbative QCD cross sections for the processes listed above. However, to make a quantitative comparison to experimental data at the realistically low photon virtuality $M \sim 1$ GeV, one has to take into account the non-perturbative spectral functions and self-energies of the quarks, anti-quark and gluons thus going beyond the leading twist. Therefore, we have derived the off-shell cross sections of $q\bar{q} \rightarrow \gamma^*$, $q\bar{q} \rightarrow \gamma^* + g$ and $qg \rightarrow \gamma^* q (qg \rightarrow \gamma^* q)$ reactions by calculating the corresponding diagrams for massive quarks and gluons, with the masses being distributed according to the DQPM self energies. The obtained off-shell elementary cross sections then have been implemented into the PHSD transport code.

In Fig. 2 (L.h.s.) we present PHSD results for the dilepton spectrum excess over the known hadronic sources as produced in $In + In$ reactions at 158 AGeV compared to the acceptance corrected data published recently by the NA60 Collaboration [10]. We find that the spectrum at invariant masses below 1 GeV is well reproduced by the $\rho$ meson yield, if a broadening of the meson spectral function in the medium is assumed [11]. Thus the result of [12] is
confirmed by the PHSD calculations. On the other hand, the spectrum at $M > 1$ GeV is shown to be dominated by the partonic sources.

It is also interesting to note that accounting for partonic dilepton sources allows to reproduce in PHSD (cf. Fig. 2, rhs) the intriguing finding of the NA60 Collaboration [14, 16] that the effective temperature of the dileptons (slope parameters) in the intermediate mass range is lower than the $T_{\text{eff}}$ of the dileptons from the hadronic phase. The softening of the transverse mass spectrum with growing invariant mass implies that the partonic channels occur dominantly before the collective radial flow has developed. In total we still underestimate the slope parameter $T_{\text{eff}}$ (cf. rhs in Fig. 2) which might be due to missing partonic initial state effects or an underestimation of partonic flow in the initial phase of the reaction. These issues are presently being addressed and will be reported in the near future.

IV. RHIC ENERGIES

In 2008, the PHENIX Collaboration has presented first dilepton data from $pp$ and $Au+Au$ collisions at Relativistic-Heavy-Ion-Collider (RHIC) energies of $\sqrt{s} = 200$ GeV [18] which show an even larger enhancement in $Au+Au$ reactions (relative to $pp$ collisions) in the invariant mass regime from 0.15 to 0.6 GeV than the data at SPS energies [17]. We recall that HSD provides a reasonable description of hadron production in $Au+Au$ collisions at $\sqrt{s} = 200$ GeV [20] such that we can directly continue with the results for $e^+e^-$ pairs which are shown in Fig. 3 for $p+p$ collisions. We find that the dilepton radiation in the elementary channel is well under control in HSD, which is equivalent to PHSD for $p+p$ reactions.

We step on with the case of inclusive $Au+Au$ collisions in comparison to the data from PHENIX [18] (Fig. 4). When including the in-medium modification scenarios for the vector mesons, we achieve a sum spectrum which is only slightly enhanced compared to the ‘free’ scenario. Whereas the total yield is quite well described in the region of the pion Dalitz decay as well as around the $\omega$ and $\phi$ mass, HSD clearly underestimates the measured spectra in the regime from 0.2 to 0.6 GeV by an average factor of 3. The low mass dilepton spectra from $Au+Au$ collisions at RHIC (from the PHENIX Collaboration) are clearly underestimated in the invariant mass range from 0.2 to 0.6 GeV in the ‘collisional broadening’ scenario as well as in the ‘dropping mass + collisional broadening’ model, i.e. when assuming a shift of the vector meson mass poles with the baryon density. We mention that our results for the low
mass dileptons are very close to the calculated spectra from van Hees and Rapp as well as Dusling and Zahed [21] (cf. the comparison in Ref. [22]). Consequently we attribute this additional low mass enhancement seen by PHENIX to non-hadronic sources and will proceed with the quantitative test of this assumption in a future publication.

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**FIG. 4:** The HSD results for the mass differential dilepton spectra in case of inclusive $Au + Au$ collisions at $\sqrt{s} = 200$ GeV in comparison to the data from PHENIX [18]. The actual PHENIX acceptance filter and mass resolution have been incorporated [19]. In the upper part the results are shown for vacuum spectral functions (for $\rho, \omega, \phi$) including the channel decompositions (see legend for the different color coding of the individual channels). The lower part shows a comparison for the total $e^+e^-$ mass spectrum in case of the ‘free’ scenario (dashed line), the ‘collisional broadening’ picture (solid line) as well as the ‘dropping mass + collisional broadening’ model (dash-dotted line). Figure taken from [11].

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