Measurements of production cross sections of the Higgs boson in the four-lepton final state in proton–proton collisions at $\sqrt{s} = 13$ TeV

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Abstract Production cross sections of the Higgs boson are measured in the $H \rightarrow ZZ \rightarrow 4\ell$ ($\ell = e, \mu$) decay channel. A data sample of proton–proton collisions at a center-of-mass energy of 13 TeV, collected by the CMS detector at the LHC and corresponding to an integrated luminosity of 137 fb$^{-1}$ is used. The signal strength modifier $\mu$, defined as the ratio of the Higgs boson production rate in the 4$\ell$ channel to the standard model (SM) expectation, is measured to be $\mu = 0.94 \pm 0.07$ (stat)$^{+0.09}_{-0.08}$ (syst) at a fixed value of $m_H = 125.38$ GeV. The signal strength modifiers for the individual Higgs boson production modes are also reported. The inclusive fiducial cross section for the $H \rightarrow 4\ell$ process is measured to be $2.84^{+0.23}_{-0.22}$ (stat)$^{+0.26}_{-0.21}$ (syst) fb, which is compatible with the SM prediction of 2.84$\pm$0.15 fb for the same fiducial region. Differential cross sections as a function of the transverse momentum and rapidity of the Higgs boson, the number of associated jets, and the transverse momentum of the leading associated jet are measured. A new set of cross section measurements in mutually exclusive categories targeted to identify production mechanisms and kinematical features of the events is presented. The results are in agreement with the SM predictions.

1 Introduction

The discovery of the Higgs boson (H) in 2012 by the ATLAS and CMS collaborations [1–3] has been a major step towards the understanding of the electroweak symmetry breaking mechanism [4–9]. Further studies by the two experiments [10–13] have shown that the properties of the new particle are consistent with the standard model (SM) expectations for the H boson.

The $H \rightarrow ZZ \rightarrow 4\ell$ decay channel ($\ell = e, \mu$) has a large signal-to-background ratio thanks to a low background rate and the complete reconstruction of the final state decay products, capitalizing on the excellent lepton momentum resolution of the CMS detector. The measurements performed using this decay channel with the LHC Run 1 data set at center-of-mass energies of 7 and 8 TeV, and the Run 2 data set at 13 TeV include the determination of the mass, the spin and the parity of the H boson [14–19], its width [20–23], the inclusive and differential fiducial cross sections [18,24–28], and the tensor structure of the H boson interaction with a pair of neutral gauge bosons in both on-shell and off-shell regions [17,19,21,29,30].

This paper presents the measurement of production cross sections in granular kinematic regions of the H boson in the $H \rightarrow ZZ \rightarrow 4\ell$ decay channel. A data sample of proton–proton (pp) collisions at a center-of-mass energy of $\sqrt{s} = 13$ TeV, collected by the CMS detector at the LHC and corresponding to an integrated luminosity of 137 fb$^{-1}$ is used. The inclusive signal strength modifier, defined as the ratio of the H boson production rate in the 4$\ell$ channel to the SM expectation, and signal strength modifiers for the individual H boson production modes are measured. The measurements of the inclusive and differential fiducial cross sections are also presented, and their compatibility with the SM predictions is tested. The present analysis is similar to that previously performed by the CMS Collaboration [18], but is based on a larger data sample.

In addition, measurements of the H boson cross sections within the simplified template cross section (STXS) framework [31–33] are also presented. The main goals of the STXS framework are to increase the reinterpretable of the precision H boson measurements and to minimize the theory dependence. This is achieved by defining exclusive kinematic regions in the H boson production phase space. The results presented within the STXS framework nonetheless depend on the SM simulation used to model the experimental acceptance of the signal processes, which could be modified in beyond the SM (BSM) scenarios. These kinematic regions, referred to as bins, are defined in different stages corresponding to increasing degrees of granularity. This paper presents
results in the STXS stage 0 where the bins correspond closely to the different H boson production mechanisms. Previous measurements of cross sections in stage 0 production bins in the $H \rightarrow 4\ell$ decay channel were already presented by the CMS Collaboration [18]. In the STXS framework, additional stages are defined by further splitting of the bins enhancing the sensitivity to possible signature of BSM physics at high transverse momentum of the H boson. Measurements of stage 0, stage 1, and stage 1.1 cross sections in the $H \rightarrow 4\ell$ decay channel were recently published by the ATLAS Collaboration [27]. The most recent refinement of STXS binning is referred to as STXS stage 1.2. This paper presents a first set of the cross section measurements in the STXS stage 1.2 bins in the $H \rightarrow 4\ell$ decay channel.

The paper is organized as follows. A brief introduction of the CMS detector is given in Sect. 2. The data, as well as the simulated signal and background samples, are described in Sect. 3. The event reconstruction and selection, the kinematic discriminants, and the categorization of the H boson candidate events are described in Sects. 4, 5, and 6, respectively. The background estimation is detailed in Sect. 7 while the signal modeling is described in Sect. 8. The experimental and theoretical systematic uncertainties are described in Sect. 9 and the results are presented in Sect. 10. Concluding remarks are given in Sect. 11.

2 The CMS detector

The central feature of the CMS apparatus is a superconducting solenoid of 6 m internal diameter, providing a magnetic field of 3.8 T. Within the solenoid volume are a silicon pixel and strip tracker, a lead tungstate crystal electromagnetic calorimeter (ECAL), and a brass and scintillator hadron calorimeter (HCAL), each composed of a barrel and two endcap sections. Forward calorimeters extend the pseudorapidity coverage provided by the barrel and endcap detectors. Muons are detected in gas-ionization chambers embedded in the steel flux-return yoke outside the solenoid.

Events of interest are selected using a two-tiered trigger system. The first level, composed of custom hardware processors, uses information from the calorimeters and muon detectors to select events at a rate of around 100 kHz within a fixed latency of about 4 $\mu$s [34]. The second level, known as the high-level trigger, consists of a farm of processors running a version of the full event reconstruction software optimized for fast processing, and reduces the event rate to around 1 kHz before data storage [35].

The candidate vertex with the largest value of summed physics-object squared transverse momentum $p_T^2$ is taken to be the primary pp interaction vertex (PV). The physics objects are the jets, clustered using the jet finding algorithm [36,37] with the tracks assigned to candidate vertices as inputs, and the associated missing transverse momentum, taken as the negative vector sum of the $p_T$ of those jets.

The electron momentum is estimated by combining the energy measurement in the ECAL with the momentum measurement in the tracker. The momentum resolution for electrons with $p_T \approx 45$ GeV from $Z \rightarrow ee$ decays ranges from 1.7% to 4.5%. It is generally better in the barrel region than in the endcaps, and also depends on the bremsstrahlung energy emitted by the electron as it traverses the material in front of the ECAL [38]. The ECAL consists of 75 848 lead tungstate crystals, which provide coverage of $|\eta| < 1.48$ in the barrel region and $1.48 < |\eta| < 3.00$ in the two endcap regions (EE). Preshower detectors consisting of two planes of silicon sensors interleaved with a total of 3$X_0$ of lead are located in front of each EE detector.

Muons are measured in the pseudorapidity range $|\eta| < 2.4$, with detection planes made using three technologies: drift tubes, cathode strip chambers, and resistive plate chambers. The single muon trigger efficiency exceeds 90% over the full $\eta$ range, and the efficiency to reconstruct and identify muons is greater than 96%. Matching muons to tracks measured in the silicon tracker results in a relative transverse momentum resolution, for muons with $p_T$ up to 100 GeV, of 1% in the barrel and 3% in the endcaps. The $p_T$ resolution in the barrel is better than 7% for muons with $p_T$ up to 1 TeV [39].

A more detailed description of the CMS detector, together with a definition of the coordinate system used and the relevant kinematic variables, can be found in Ref. [40].

3 Data and simulated samples

This analysis is based on the pp collision data collected by the CMS detector at the LHC in 2016, 2017, and 2018 with integrated luminosities of 35.9, 41.5, and 59.7 fb$^{-1}$, respectively [41–43]. The collision events are selected by high-level trigger algorithms that require the presence of leptons passing loose identification and isolation requirements. The main triggers select either a pair of electrons or muons, or an electron and a muon. The minimal transverse momentum of the leading and subleading leptons changed throughout the years to account for the different data-taking conditions and is summarized in Table 1.

To maximize the coverage of the $H \rightarrow 4\ell$ phase space, triggers requiring three leptons with relaxed transverse momenta thresholds and no isolation requirement are also used, as are isolated single-electron and single-muon triggers. The overall trigger efficiency for simulated signal events that pass the full event selection (described in Sect. 4) is larger than 99%. The trigger efficiency is derived from data using a sample of $4\ell$ events collected by the single-lepton triggers and a method based on the “tag and probe”
Table 1 The minimal \( p_T \) of the leading/subleading leptons for the main di-electron (e/e), di-muon (\( \mu/\mu \)), and electron-muon (e/\( \mu, \mu/e \)) high-level trigger algorithms used in the \( H \to 4\ell \) analysis in 2016, 2017, and 2018.

|        | e/e (GeV) | \( \mu/\mu \) (GeV) | e/\( \mu, \mu/e \) (GeV) |
|--------|-----------|----------------------|--------------------------|
| 2016   | 17/12     | 17/8                 | 17/8, 8/23               |
| 2017   | 23/12     | 17/8                 | 23/8, 12/23              |
| 2018   | 23/12     | 17/8                 | 23/8, 12/23              |

Monte Carlo (MC) simulation samples for the signals and the relevant background processes are used to evaluate the signal shape, estimate backgrounds, optimize the event selection, and evaluate the acceptance and systematic uncertainties. The SM H boson signals are simulated at next-to-leading order (NLO) in perturbative QCD (pQCD) with the POWHEG 2.0 [44–46] generator for the five main production processes: gluon fusion (ggH) [47], vector boson fusion (VBF) [48], associated production with a vector boson (VH, where \( V \) is a W or a Z boson) [49], and associated production with a pair of top quarks (t\( \bar{t}H \)) [50]. The ZH production occurs in two ways, \( q\bar{q} \to ZH \) and a much smaller contribution from \( g \to ZH \), which is simulated at leading order (LO) using JHUGEN 7.3.0 [51–55]. In addition to the five main production processes, the contributions due to H boson production in association with a single top quark (tH) and either a quark (t\( Hq \)) or a W boson (tHW) are simulated at LO using JHUGEN 7.0.2 and MadGraph5_aMC@NLO 2.2.2 [56], respectively. The associated production with a pair of bottom quarks (b\( b \bar{H} \)) is simulated at LO with JHUGEN 7.0.2. In all cases, the decay of the H boson to four leptons is modeled with JHUGEN 7.0.2. The theoretical predictions used for the various production and decay modes can be found in Refs. [57–79] and are summarized in Ref. [32].

The ZZ background contribution from quark-antiquark annihilation is simulated at NLO pQCD with POWHEG 2.0 [80], while the \( gg \to ZZ \) process is generated at LO with MCFM 7.0.1 [81]. The WZ background and the triboson backgrounds ZZZ, WZZ, and WWZ are modeled at NLO using MadGraph5_aMC@NLO 2.4.2. The smaller t\( T\bar{T} \), t\( W\bar{W} \), and t\( t\bar{ZZ} \) backgrounds are simulated at LO with MadGraph5_aMC@NLO 2.4.2. The events containing Z bosons with associated jets (Z+jets) are simulated at NLO with MadGraph5_aMC@NLO 2.4.2 and the t\( t\bar{t} \) background is simulated at NNLO with POWHEG 2.0. The reducible background determination does not rely on the MC but is based on data, as described in Sect. 7.2.

All signal and background event generators are interfaced with PYTHIA 8.230 [82] using the CUETP8M1 tune [83] for the 2016 data-taking period and the CP5 tune [84] for the 2017 and 2018 data-taking periods, to simulate the multi-parton interaction and hadronization effects. The NNPDF3.0 set of parton distribution functions (PDFs) is used [85]. The generated events are processed through a detailed simulation of the CMS detector based on GEANT4 [86,87] and are reconstructed with the same algorithms that are used for data. The simulated events include overlapping pp interactions (pileup) and have been reweighted so that the distribution of the number of interactions per LHC bunch crossing in simulation matches that observed in data.

4 Event reconstruction and selection

The particle-flow (PF) algorithm [88] aims to reconstruct and identify each individual particle (PF candidate) in an event, with an optimized combination of information from the various elements of the CMS detector. The energy of photons is obtained from the ECAL measurement. The energy of electrons is determined from a combination of the electron momentum at the PV as determined by the tracker, the energy of the corresponding ECAL cluster, and the energy sum of all bremsstrahlung photons spatially compatible with originating from the electron track. The energy of muons is obtained from the curvature of the corresponding track. The energy of charged hadrons is determined from a combination of their momentum measured in the tracker and the matching ECAL and HCAL energy deposits, corrected for the response function of the calorimeters to hadronic showers. Finally, the energy of neutral hadrons is obtained from the corresponding ECAL and HCAL energies.

The missing transverse momentum vector \( \vec{p}_T^{\text{miss}} \) is computed as the negative vector sum of the transverse momenta of all the PF candidates in an event, and its magnitude is denoted as \( p_T^{\text{miss}} \) [89]. The \( \vec{p}_T^{\text{miss}} \) is modified to account for corrections to the energy scale of the reconstructed jets in the event.

Muons with \( p_T^\mu > 5 \text{ GeV} \) are reconstructed within the geometrical acceptance, corresponding to the region \( |\eta^\mu| < 2.4 \), by combining information from the silicon tracker and the muon system [39]. The matching between the inner and outer tracks proceeds either outside-in, starting from a track in the muon system, or inside-out, starting from a track in the silicon tracker. Inner tracks that match segments in only one or two stations of the muon system are also considered because they may belong to very low-\( p_T \) muons that do not have sufficient energy to penetrate the entire muon system. The muons are selected among the reconstructed muon track.
candidates by applying minimal requirements on the track in both the muon system and the inner tracker system, and taking into account the compatibility with small energy deposits in the calorimeters.

To discriminate between prompt muons from Z boson decay and those arising from electroweak (EW) decays of hadrons within jets, an isolation requirement of $I^\mu < 0.35$ is imposed, where the relative isolation is defined as

$$I^\mu \equiv \left( \sum p_T^{\text{charged}} + \max \left[ 0, \sum p_T^{\text{neutral}} \right] + \sum p_T^\gamma - p_T^{\mu, \text{PU}} \right) / p_T^\mu. \quad (1)$$

In Eq. (1), $\sum p_T^{\text{charged}}$ is the scalar sum of the transverse momenta of charged hadrons originating from the chosen PV of the event. The quantities $\sum p_T^{\text{neutral}}$ and $\sum p_T^\gamma$ are the scalar sums of the transverse momenta for neutral hadrons and photons, respectively. The isolation sums involved are all restricted to a volume bound by a cone of angular radius $\Delta R = 0.3$ around the muon direction at the PV, where the angular distance between two particles $i$ and $j$ is $\Delta R(i, j) = \sqrt{(\eta^i - \eta^j)^2 + (\phi^i - \phi^j)^2}$. Since the isolation variable is particularly sensitive to energy deposits from pileup interactions, a $p_T^{\mu, \text{PU}}$ contribution is subtracted, defined as $p_T^{\mu, \text{PU}} \equiv 0.5 \sum p_T^{\gamma, \text{PU}}$, where $i$ runs over the charged hadron PF candidates not originating from the PV, and the factor of 0.5 corrects for the different fraction of charged and neutral particles in the cone [90].

Electrons with $p_T^e > 7$ GeV are reconstructed within the geometrical acceptance, corresponding to the pseudorapidity region $|\eta^e| < 2.5$ [38]. Electrons are identified using a multivariate discriminant which includes observables sensitive to the presence of bremsstrahlung along the electron trajectory, the geometrical and momentum–energy matching between the electron trajectory and the associated cluster in the ECAL, the shape of the electromagnetic shower in the ECAL, and variables that discriminate against electrons originating from photon conversions. Instead of an additional isolation requirement, similar to the one for muons, the electron multivariate discriminant also includes the isolation sums described above ($\sum p_T^{\text{charged}}$, $\sum p_T^{\text{neutral}}$, and $\sum p_T^\gamma$) but computed around the electron direction. The inclusion of isolation sums helps suppressing electrons originating from electroweak decays of hadrons within jets [91] and has a better performance than a simple requirement on the relative isolation observable. The package XGBOOST [92] is used for the training and optimization of the multivariate discriminant employed for electron identification and isolation. The training is performed with simulated events that are not used at any other stage of the analysis. Events are divided into six regions defined by two transverse momentum ranges (7–10 GeV and > 10 GeV) and three pseudorapidity regions: central barrel ($|\eta^e| < 0.8$), outer barrel (0.8 < $|\eta^e| < 1.479$), and endcaps (1.479 < $|\eta^e| < 2.5$). Separate training is performed for the three different data-taking periods and selection requirements are determined such that the signal efficiency remains the same for all three periods.

The effect of the final-state radiation (FSR) from leptons is recovered as follows. Bremsstrahlung photons already associated to electrons in the reconstruction step are not considered in this procedure. Photons reconstructed by the PF algorithm within $|\eta^\gamma| < 2.4$ are considered as FSR candidates if they satisfy the conditions $p_T^\gamma > 2$ GeV and $I^\gamma < 1.8$, where the photon relative isolation $I^\gamma$ is defined as for the muon in Eq. (1). Every such photon is associated to the closest selected lepton in the event. Photons that do not satisfy the requirements $\Delta R(\gamma, \ell)/(p_T^\gamma)^2 < 0.012$ GeV$^{-2}$ and $\Delta R(\gamma, \ell) < 0.5$ are discarded. The lowest-$\Delta R(\gamma, \ell)/(p_T^\gamma)^2$ photon candidate of every lepton, if any, is retained. The photons thus identified are excluded from the isolation computation of the muons selected in the event.

In order to suppress muons from in-flight decays of hadrons and electrons from photon conversions, leptons are rejected if the ratio of their impact parameter in three dimensions, computed with respect to the PV position, to their uncertainty is greater or equal to four.

The momentum scale and resolution of electrons and muons are calibrated in bins of $p_T^e$ and $\eta^e$ using the decay products of known dilepton resonances as described in Refs. [38, 39]. A “tag and probe” technique [93] based on samples of Z boson events in data and simulation is used to measure the efficiency of the reconstruction and selection for prompt electrons and muons in several bins of $p_T^e$ and $\eta^e$. The difference in the efficiencies measured in simulation and data is used to rescale the yields of selected events in the simulated samples.

For each event, hadronic jets are clustered from the reconstructed particles using the infrared- and collinear-safe anti-$k_T$ algorithm [36, 37] with a distance parameter of 0.4. The jet momentum is determined as the vectorial sum of all particle momenta in the jet, and is found from simulation to be within 5–10% of the true momentum over the whole $p_T$ spectrum and detector acceptance. Additional pp interactions within the same or nearby bunch crossings can contribute extra tracks and calorimetric energy depositions to the jet. To mitigate this effect, tracks identified as originating from pileup vertices are discarded and an offset correction is applied to correct for the remaining contributions. Jet energy corrections are derived from simulation to match that of particle level jets on average. In situ measurements of the momentum balance in dijet, photon + jet, Z+ jet, and multijet events are used to account for any residual differences in jet energy scale in data and simulation [94]. Jet energies in simulation are smeared to match the resolution in data. The jet energy resolution amounts typically to 16% at 30 GeV, 8%
at 100 GeV, and 4% at 1 TeV. Additional selection criteria are applied to remove jets potentially dominated by anomalous contributions from various subdetector components or reconstruction failures. To be considered in the analysis, jets must satisfy the conditions \( p_T^{\text{jet}} > 30 \text{ GeV} \) and \( |\eta^{\text{jet}}| < 4.7 \), and be separated from all selected lepton candidates and any selected FSR photons by \( \Delta R(\ell/\gamma, \text{jet}) > 0.4 \). Jets are also required to pass the tight identification criteria and the tight working point of pileup jet identification described in Ref. [90].

For event categorization, jets are tagged as b jets using the DeepCSV algorithm [95], which combines information about impact parameter significance, secondary vertex, and jet kinematics. Data to simulation scale factors for the b tagging efficiency are applied as a function of jet \( p_T, \eta \), and flavor.

The event selection is designed to extract signal candidates from events containing at least four well-identified and isolated leptons, each originating from the PV and possibly accompanied by an FSR photon candidate. In what follows, unless otherwise stated, FSR photons are included in invariant mass computations.

First, Z candidates are formed with pairs of leptons of the same flavor and opposite-charge (\( e^+e^-, \mu^+\mu^- \)) that pass the requirement \( 12 < m_{\ell^+\ell^-} < 120 \text{ GeV} \). They are then combined into ZZ candidates, wherein we denote as \( Z_1 \) the Z candidate with an invariant mass closest to the nominal Z boson mass [96], and as \( Z_2 \) the other one. The flavors of the involved leptons define three mutually exclusive subchannels: 4e, 4\( \mu \), and 2e2\( \mu \).

To be considered for the analysis, ZZ candidates have to pass a set of kinematic requirements that improve the sensitivity to H boson decays. The \( Z_1 \) invariant mass must be larger than 40 GeV. All leptons must be separated in angular space by at least \( \Delta R(\ell_i, \ell_j) > 0.02 \). At least two leptons are required to have \( p_T > 10 \text{ GeV} \) and at least one is required to have \( p_T > 20 \text{ GeV} \). In the 4\( \mu \) and 4e subchannels, where an alternative \( Z_2 \) can be built out of the same four leptons, we discard candidates with \( m_{Z_2} < 12 \text{ GeV} \) if \( Z_2 \) is closer to the nominal Z boson mass than \( Z_1 \) is. This rejects events that contain an on-shell Z and a low-mass dilepton resonance. To further suppress events with leptons originating from hadron decays in jet fragmentation or from the decay of low-mass resonances, all four opposite-charge lepton pairs that can be built with the four leptons (irrespective of flavor) are required to satisfy the condition \( m_{\ell^+\ell^-} > 4 \text{ GeV} \), where selected FSR photons are disregarded in the invariant mass computation. Finally, the four-lepton invariant mass \( m_{4\ell} \) must be larger than 70 GeV, which defines the mass range of interest for the subsequent steps of the analysis.

In events where more than one ZZ candidate passes the above selection, the candidate with the highest value of \( D_{\text{bkg}}^{\text{kin}} \) (defined in Sect. 5) is retained, except if two candidates consist of the same four leptons, in which case the candidate with the \( Z_1 \) mass closest to the nominal Z boson mass is retained.

### 5 Kinematic discriminants

The full kinematic information from each event using either the H boson decay products and/or the associated particles in the H boson production is extracted by means of matrix element calculations and is used to form several kinematic discriminants. These computations rely on the MELA package [51–53,55] and exploit the \( \text{JHUGEN} \) matrix elements for the signal and the \( \text{MCFM} \) matrix elements for the background. Both the H boson decay kinematics and the kinematics of the associated production of \( H + 1\text{ jet}, H + 2\text{ jets}, VBF, ZH, \) and WH are explored. The full event kinematics is described by decay observables \( \vec{\Omega}^{H+4\ell} \) or observables describing the associated production \( \vec{\Omega}^{H+ij} \), which may or may not include the \( H \to 4\ell \) decay kinematic information depending on the use case. The definition of these observables can be found in Refs. [51–53].

Two types of kinematic discriminants are exploited in the \( H \to 4\ell \) analysis. First we construct the three categorization discriminants in order to classify signal events into exclusive categories as defined in Sect. 6.2. Categorization discriminants are designed to increase the purity of the targeted production mechanism in a dedicated event category. In addition, we define another set of three kinematic discriminants that are taken as an observable in the two-dimensional likelihood fits carried out to extract the results, as described in Sect. 10. These kinematic discriminants are designed to separate the target H boson production mechanism from its dominant background.

Categorization discriminants are calculated following the prescription in Refs. [18,21,97]. The discriminants sensitive to the VBF signal topology with two associated jets, the VBF signal topology with one associated jet, and the VH (either \( ZH \) or \( WH \)) signal topology with two associated jets are:

\[
\begin{align*}
    D_{\ell}^{\text{VBF}}^{2\text{jet}} &= \left[1 + \frac{P_{\text{Hij}}(\vec{\Omega}^{H+ij}[m_4])}{P_{\text{VBF}}(\vec{\Omega}^{H+ij}[m_4])}\right]^{-1} \\
    D_{\ell}^{\text{VBF}}^{1\text{jet}} &= \left[1 + \frac{P_{\text{Hij}}(\vec{\Omega}^{H+ij}[m_4])}{\int d\eta P_{\text{VBF}}(\vec{\Omega}^{H+ij}[m_4])}\right]^{-1} \\
    D_{\ell}^{\text{WH}}^{2\text{jet}} &= \left[1 + \frac{P_{\text{Hij}}(\vec{\Omega}^{H+ij}[m_4])}{P_{\text{WH}}(\vec{\Omega}^{H+ij}[m_4])}\right]^{-1} \\
    D_{\ell}^{\text{ZH}}^{2\text{jet}} &= \left[1 + \frac{P_{\text{Hij}}(\vec{\Omega}^{H+ij}[m_4])}{P_{\text{ZH}}(\vec{\Omega}^{H+ij}[m_4])}\right]^{-1}
\end{align*}
\]
where \( \mathcal{P}_{\text{VBF}}, \mathcal{P}_{\text{Hjj}}, \mathcal{P}_{\text{Hj}}, \) and \( \mathcal{P}_{\text{VH}} \) are the probabilities for the VBF process, the ggH process in association with two jets (combination of gg/q\bar{q}/q\bar{q} parton collisions producing H + 2 jets), the ggH process in association with one jet (H + 1 jet), and the VH process, respectively. The quantity \( \int d\eta \mathcal{P}_{\text{VBF}} \) is the integral of the two-jet VBF matrix element probability over the \( \eta \) values of the unobserved jet, with the constraint that the total transverse momentum of the H + 2 jets system is zero. The discriminant \( \mathcal{D}_{2\text{jet}}^{\text{VH}} \), used for event categorization, is defined as the maximum value of the two discriminants, \( \mathcal{D}_{2\text{jet}}^{\text{VH}} = \max(\mathcal{D}_{2\text{jet}}^{\text{VBF}}, \mathcal{D}_{2\text{jet}}^{\text{VH}}) \).

A set of three discriminants used in the likelihood fits is calculated as in Refs. [17, 18]. The discriminant sensitive to the \( gg/q\bar{q} \to 4\ell \) process exploits the kinematics of the four-lepton decay system. It is used in most of the event categories described in Sect. 6 to separate signal from background and is defined as:

\[
\mathcal{P}_{\text{bkg}}^{\text{kin}} = \left[ 1 + \frac{\mathcal{P}_{\text{bkg}}^{\text{gg}}(\mathcal{\Omega}_{\text{H} \to 4\ell} | m_{4\ell})}{\mathcal{P}_{\text{bkg}}^{\text{sig}}(\mathcal{\Omega}_{\text{H} \to 4\ell} | m_{4\ell})} \right]^{-1},
\]

where \( \mathcal{P}_{\text{bkg}}^{\text{gg}} \) is the probability for the signal and \( \mathcal{P}_{\text{bkg}}^{\text{sig}} \) is the probability for the dominant q\bar{q} \to 4\ell background process, calculated using the LO matrix elements. In the VBF-2jet-tagged and VH-hadronic-tagged event categories (defined in Sect. 6.2), the background includes the QCD production of ZZ/Z\gamma* /\gamma*\gamma* \to 4\ell in association with two jets, the EW background from the vector boson scattering (VBS), as well as the triboson (VVV) production process. We therefore use dedicated production-dependent discriminants based on the kinematics of the four-lepton decay and information from the associated jets (noted with VBF+ or VH+), defined as:

\[
\mathcal{D}_{\text{bkg}}^{\text{VBF+dec}} = \left[ 1 + \mathcal{c}^{\text{VBF}}(m_{4\ell}) \frac{\mathcal{P}_{\text{bkg}}^{\text{EW}}(\mathcal{\Omega}_{\text{H} \to 4\ell} | m_{4\ell}) + \mathcal{P}_{\text{bkg}}^{\text{QCD}}(\mathcal{\Omega}_{\text{H} \to 4\ell} | m_{4\ell})}{\mathcal{P}_{\text{sig}}^{\text{EW}}(\mathcal{\Omega}_{\text{H} \to 4\ell} | m_{4\ell})} \right]^{-1},
\]

\[
\mathcal{D}_{\text{bkg}}^{\text{VH+dec}} = \left[ 1 + \mathcal{c}^{\text{VH}}(m_{4\ell}) \frac{\mathcal{P}_{\text{bkg}}^{\text{EW}}(\mathcal{\Omega}_{\text{H} \to 4\ell} | m_{4\ell}) + \mathcal{P}_{\text{bkg}}^{\text{QCD}}(\mathcal{\Omega}_{\text{H} \to 4\ell} | m_{4\ell})}{\mathcal{P}_{\text{sig}}^{\text{EW}}(\mathcal{\Omega}_{\text{H} \to 4\ell} | m_{4\ell})} \right]^{-1},
\]

where \( \mathcal{P}_{\text{sig}}^{\text{EW}} \) is the probability for the VBF and VH signal, \( \mathcal{P}_{\text{bkg}}^{\text{EW}} \) is the probability for the VBS and VVV background processes, and \( \mathcal{P}_{\text{bkg}}^{\text{QCD}} \) is the probability for ZZ/Z\gamma* /\gamma*\gamma* \to 4\ell QCD production in association with two jets. The quantity \( \mathcal{c}^{P}(m_{4\ell}) \) for category \( p \) is the \( m_{4\ell} \)-dependent parameter that allows to change the relative normalization of the EW probabilities, separately for the VBF and VH topologies. For each slice of \( m_{4\ell} \), the distributions of the signal and background discriminants are plotted, and the \( \mathcal{c}^{P}(m_{4\ell}) \) value is determined in such a way that the two distributions cross at 0.5. This procedure allows rescaling of the distributions for the linear-scale binning of the templates used in the likelihood fits described in Sect. 10.

### 6 Event categorization

In order to improve the sensitivity to the H boson production mechanisms, the selected events are classified into mutually exclusive categories based on the features of the reconstructed objects associated with the H \( \to 4\ell \) candidates. Event categorization is organized in two steps with increasing granularity of the categories. First step is primarily designed to separate the ggH, VBF, VH, and ttH processes. There is little sensitivity to b\bar{b}H or tH, even though these production modes are considered explicitly in the analysis. The reconstructed event categories from the first step are further subdivided (as discussed in Sect. 6.2) in order to study each production mechanism in more detail. This subdivision is carried out by matching the recommended binning of the framework of STXS described in the following section.

#### 6.1 STXS production bins

The STXS framework has been adopted by the LHC experiments as a common framework for studies of the H boson. It has been developed to define fine-grained measurements of the H boson production modes in various kinematic regions, and to reduce the theoretical uncertainties that are folded into the measurements. It also allows for the use of advanced categorization techniques and provides a common scheme for combining measurements in different decay channels or by different experiments. The regions of phase space defined by this framework are referred to as production bins and are determined by using generator-level information for H bosons with rapidity \( |y_H| < 2.5 \). Generator-level jets are defined as anti-\( k_T \) jets with a distance parameter of 0.4 and a \( p_T \) threshold of 30 GeV; no requirement is placed on the generator-level leptons.

The STXS framework has been designed to complement the Run I measurements of the production signal strength modifiers and fiducial differential cross sections of the H boson by combining their advantages. The sensitivity to theoretical uncertainties in the signal strength modifier results is suppressed by excluding dominant theoretical uncertainties causing production bin migration effects from the STXS measurements. They are included only when comparing the results with the theoretical predictions. In contrast to the fiducial differential cross section measurements, in the STXS framework measurements are optimized for sensitivity by means of event categories and matrix element discriminants.
To account for the evolving experimental sensitivity, different stages of production bins with increasing granularity are developed.

The stage 0 production bins are called $ggH$, $qqH$, $VH-1\text{lep}$, and $ttH$ and are designed to closely match the main $H$ boson production mechanisms. The $ggH$ bin includes the EW production of the $H$ boson in association with two quarks from either VBF or VH events with hadronic decays of the vector boson $V$. The $VH-1\text{lep}$ production bin includes VH events with leptonic decays of the vector boson $V$. The low rate $b\bar{b}H$ and $tH$ production processes are considered together with the $ggH$ and $ttH$ production bins, respectively. In this analysis, a modified version of the stage 0 production bins is also studied, where instead of $VH-1\text{lep}$ and $qqH$ bins we define the $WH$, $ZH$, and $VBF$ bins that map the H boson production mechanisms without the splitting of the VH events in leptonic and hadronic decays.

Stage 1 of the STXS framework was designed by further splitting the bins from the stage 0, one of the main motives being the enhanced sensitivity to possible signatures of BSM physics. This is achieved by dividing stage 0 bins with additional requirements on generator-level quantities that include the transverse momentum of the $H$ boson ($p_T^H$), the number of associated jets ($N^b$), the dijet invariant mass ($m_{jj}$), the transverse momentum of the $H$ boson and the leading jet ($p_T^{Hj_1}$), and the transverse momentum of the $H$ boson and the two leading jets ($p_T^{Hj_1j_2}$). These bins were designed in order to maximize sensitivity to new physics while also taking into account the current experimental sensitivity limited mostly by the amount of collected data. The most recent set of bins defined in the STXS framework is referred to as stage 1.2. This paper presents a first set of cross section measurements in the $H \rightarrow 4\ell$ channel for the stage 1.2 of the STXS framework. However, several stage 1.2 production bins are merged as the full set of bins cannot be measured with the current data sample. The merging scheme results in 19 production bins; it is illustrated in Fig. 1 and discussed in more detail below.

The $ggH$ production process is split into events with $p_T^H < 200\text{ GeV}$ and $p_T^H > 200\text{ GeV}$. The events with $p_T^H > 200\text{ GeV}$ are placed into one single production bin called $ggH/p_T^H > 200$. The events with $p_T^H < 200\text{ GeV}$ are split in events with zero, one, and two or more jets. The events with zero or one jets are split into the following production bins according to the $H$ boson $p_T$: $ggH-0j/p_T[0, 10]$, $ggH-0j/p_T[10, 200]$, $ggH-1j/p_T[0, 60]$, $ggH-1j/p_T[60, 120]$, and $ggH-1j/p_T[120, 200]$. The events with two or more jets are split according to the dijet invariant mass as follows. The events with $m_{jj} < 350\text{ GeV}$ are split into three production bins according to the $H$ boson $p_T$: $ggH-2j/p_T[0, 60]$, $ggH-2j/p_T[60, 120]$, and $ggH-2j/p_T[120, 200]$. The events with $m_{jj} > 350\text{ GeV}$ are all placed into one production bin $ggH-2j/m_{jj} > 350$, which merges four bins originally suggested in stage 1.2 of the STXS framework.

The merging scheme of the electroweak $qqH$ production bins is as follows. The events with zero jets, one jet, or with two or more jets with $m_{jj} < 60\text{ GeV}$ or $120 < m_{jj} < 350\text{ GeV}$ correspond to production bins with insufficient statistics; they are all merged into one bin called $qqH-\text{rest}$. The events with two or more jets and $60 < m_{jj} < 120\text{ GeV}$ are placed in the $qqH-2j/m_{jj}[60, 120]$ bin. The events with two or more jets and $m_{jj} > 350\text{ GeV}$ are split into events with $p_T^H < 200\text{ GeV}$ and $p_T^H > 200\text{ GeV}$. The events with $p_T^H > 200\text{ GeV}$ are placed into one single production bin called $qqH-2j/p_T^H/p_T > 200$. The events with $p_T^H < 200\text{ GeV}$ and $p_T^{Hj} < 25\text{ GeV}$ are split into two production bins, $qqH-2j/m_{jj}[350, 700]$ and $qqH-2j/m_{jj} > 700$, and otherwise if $p_T^{Hj} > 25\text{ GeV}$ are merged in a single bin called $qqH-3j/m_{jj} > 350$.

The three production processes $qq\gamma' \rightarrow WH$, $gg \rightarrow ZH$, and $qq\bar{q} \rightarrow ZH$ are combined to build $VH-1\text{lep}$ reduced stage 1.2 production bins. Several proposed production bins are merged into just two bins according to the $p_T$ of the $H$ boson: $VH-1\text{lep}/p_T[0, 150]$ and $VH-1\text{lep}/p_T > 150$.

In stage 1.2 of the STXS framework the $ttH$ stage 0 production bin is split in five different bins according to the $p_T$ of the $H$ boson. Because of the very low expected yields all these bins are merged into a single bin that includes the $tH$ production process as well.

Finally, in stage 1.2 the $bb\bar{b}H$ production process, which has small cross section, is classified in the $ggH-0j/p_T[10, 200]$ production bin.

The first measurement of STXS stage 1.2 cross sections was recently performed by the CMS Collaboration [98].

6.2 Reconstructed event categories

In order to be sensitive to different production bins, the $ZZ$ candidates that pass the event selection described in Sect. 4 are classified into several dedicated reconstructed event categories. The category definitions are based on the multiplicity of jets, b-tagged jets, and additional leptons in the event. Additional leptons are not involved in the $ZZ$ candidate selection but, if present, should satisfy the identification, vertex compatibility, and isolation requirements. Requirements on the categorization discriminants described in Sect. 5, the invariant mass of the two leading jets, and the transverse momentum of the $ZZ$ candidate are also exploited.

The event categorization is carried out in two steps. In the first step, the $ZZ$ candidates are split into seven initial categories to target the main $H$ boson production mechanisms corresponding to the stage 0 production bins. The first step of the categorization closely follows the analysis strategy from...
Fig. 1 Binning of the gluon fusion production process, the electroweak production process (combines VBF and VH with hadronic V decay), the VH production process with leptonic V decay (combining WH, ZH, and gluon fusion ZH production), and the t\(t\bar{t}\)H production process in the merged stage 1.2 of the STXS framework used in the \(H \rightarrow ZZ \rightarrow 4\ell\) analysis.

The previous publication [18]. To ensure exclusive categories, an event is considered for the subsequent category only if it does not satisfy the requirements of the previous one.

In the first categorization step, the following criteria are applied:

- The VBF-2jet-tagged category requires exactly 4 leptons. In addition there must be either 2 or 3 jets of which at most 1 is b-tagged, or at least 4 jets and no b-tagged jets. Finally, \(D_{VBF}^{2\text{jet}} > 0.5\) is required.
- The VH-hadronic-tagged category requires exactly 4 leptons. In addition there must be 2 or 3 jets with no b-tagging requirements, or at least 4 jets and no b-tagged jets. Finally, \(D_{VH}^{2\text{jet}} > 0.5\) is required.
- The VH-leptonic-tagged category requires no more than 3 jets and no b-tagged jets in the event, and exactly 1 additional lepton or 1 additional pair of opposite sign, same flavor leptons. This category also includes events with no jets and at least 1 additional lepton.
- The \(t\bar{t}\)H-hadronic-tagged category requires at least 4 jets, of which at least 1 is b-tagged, and no additional leptons.
- The \(t\bar{t}\)H-leptonic-tagged category requires at least 1 additional lepton in the event.
- The VBF-1jet-tagged category requires exactly 4 leptons, exactly 1 jet and \(D_{VBF}^{1\text{jet}} > 0.7\).
- The untagged category consists of the remaining events.

Reconstructed events are further subdivided in the second step of the categorization that is designed to closely match the merged stage 1.2 production bins described in the previous section. In the second categorization step, the untagged, VBF-2jet-tagged, VH-hadronic-tagged, and VH-leptonic-tagged categories are further split exploiting additional variables like the invariant mass of the two leading jets and the transverse momentum of the ZZ candidate. A total number of twenty-two reconstructed event categories is defined and details of the categorization are presented in Table 2.
Table 2  Event categorization criteria of the $H \to 4\ell$ analysis targeting stage 1.2 STXS production bins. Events from the first step of the categorization are further classified based on the kinematical properties listed in the table. A dash indicates no requirement

| Reconstructed event category | 1st categorization step | Number of jets | Kinematical requirements ( GeV ) | Targeted production bin |
|-----------------------------|-------------------------|----------------|-------------------------------|-------------------------|
| Untagged-0j- $p_T^{4\ell}$ [0, 10] | Untagged | 0 | $0 < p_T^{4\ell} < 10$ | $ggH$-0j/p_T=0.10 |
| Untagged-0j- $p_T^{4\ell}$ [10, 200] | Untagged | 0 | $10 < p_T^{4\ell} < 200$ | $ggH$-0j/p_T=10, 200 |
| Untagged-1j- $p_T^{4\ell}$ [0, 60] | Untagged | 1 | $0 < p_T^{4\ell} < 60$ | $ggH$-1j/p_T=0.60 |
| Untagged-1j- $p_T^{4\ell}$ [60, 120] | Untagged | 1 | $60 < p_T^{4\ell} < 120$ | $ggH$-1j/p_T=60, 120 |
| Untagged-1j- $p_T^{4\ell}$ [120, 200] | Untagged | 1 | $120 < p_T^{4\ell} < 200$ | $ggH$-1j/p_T=120, 200 |
| Untagged-2j- $p_T^{4\ell}$ [0, 60] | Untagged | 2 | $0 < p_T^{4\ell} < 60, m_{jj} < 350$ | $ggH$-2j/p_T=0.60 |
| Untagged-2j- $p_T^{4\ell}$ [60, 120] | Untagged | 2 | $60 < p_T^{4\ell} < 120, m_{jj} < 350$ | $ggH$-2j/p_T=60, 120 |
| Untagged-2j- $p_T^{4\ell}$ [120, 200] | Untagged | 2 | $120 < p_T^{4\ell} < 200, m_{jj} < 350$ | $ggH$-2j/p_T=120, 200 |
| Untagged-2j- $m_{jj} > 350$ | Untagged | 2 | $m_{jj} > 350$ | $ggH$-2j/m_{jj} > 350 |
| VBF-1jet-tagged | VBF-1jet-tagged | – | – | $qqH$-rest |
| VBF-2jet-tagged-$m_{jj}$[350, 700] | VBF-2jet-tagged | – | $p_T^{4\ell} < 200, p_T^{4(ij)} < 25, 350 < m_{jj} < 700$ | $qqH$-2j/m_{jj}[350, 700] |
| VBF-2jet-tagged-$m_{jj} > 700$ | VBF-2jet-tagged | – | $p_T^{4\ell} < 200, p_T^{4(ij)} < 25, m_{jj} > 700$ | $qqH$-2j/m_{jj} > 700 |
| VBF-3jet-tagged-$m_{jj} > 350$ | VBF-3jet-tagged | – | $p_T^{4\ell} < 200, p_T^{4(ij)} > 25, m_{jj} > 350$ | $qqH$-3j/m_{jj} > 350 |
| VBF-2jet-tagged-$p_T^{4\ell} > 200$ | VBF-2jet-tagged | – | $p_T^{4\ell} > 200, m_{jj} > 350$ | $qqH$-2j/p_T=200 |
| VBF-rest | VBF-2jet-tagged | – | $m_{jj} < 350$ | $qqH$-rest |
| VH-hadronic-tagged-$m_{jj}$[60, 120] | VH-hadronic-tagged | – | $60 < m_{jj} < 120$ | $qqH$-2j/m_{jj}[60, 120] |
| VH-rest | VH-hadronic-tagged | – | $m_{jj} < 60$ or $m_{jj} > 120$ | $qqH$-rest |
| VH-leptonic-tagged-$p_T^{4\ell}$[0, 150] | VH-leptonic-tagged | – | $p_T^{4\ell} < 150$ | $VH$-lep/p_T=0.150 |
| VH-leptonic-tagged-$p_T^{4\ell} > 150$ | VH-leptonic-tagged | – | $p_T^{4\ell} > 150$ | $VH$-lep/p_T=150 |
| tH-leptonic-tagged | tH-leptonic-tagged | – | – | tth |
| tH-hadronic-tagged | tH-hadronic-tagged | – | – | tth |
7 Background estimation

7.1 Irreducible backgrounds

The irreducible background to the H boson signal in the $4\ell$ channel, which comes from the production of ZZ via q\bar{q} annihilation or gluon fusion, is estimated using simulation. The fully differential cross section for the q\bar{q} → ZZ process is computed at NNLO [99], and the NNLO/NLO K factor as a function of $m_{ZZ}$ is applied to the powheg sample. This K factor varies from 1.0 to 1.2 and is 1.1 at $m_{ZZ} = 125$ GeV. Additional NLO electroweak corrections that depend on the initial state quark flavor and kinematics are also applied in the region $m_{ZZ} > 2m_Z$ following the prescription in Ref. [100].

The production of ZZ via gluon fusion contributes at NNLO in pQCD. It has been shown that the soft collinear approximation is able to describe the cross section for this process and the interference term at NNLO [101]. Further calculations also show that the K factors are very similar at NLO for signal and background [102] and at NNLO for signal and interference terms [103]. Therefore, the same K factor is used for signal and background [104]. The NNLO K factor for the signal is obtained as a function of $m_{ZZ}$ using the hnnlo v2 program [105–107] by calculating the NNLO and LO gg → H → $2\ell 2\ell'$ cross sections for the H boson decay width of 4.07 MeV and taking their ratios. The NNLO/LO K factor for gg → ZZ varies from $\approx$2.0 to 2.6 and is 2.27 at $m_{ZZ} = 125$ GeV; a systematic uncertainty of 10% is assigned to it when applied to the background process.

The triboson background processes ZZZ, WZZ, and WWZ, as well as t\bar{t}Z, t\bar{t}WW, and t\bar{t}ZZ are also considered. These rare backgrounds are all estimated from simulation and are jointly referred to as the EW backgrounds. Simulated samples are used to obtain shapes of the four-lepton invariant mass that are later used to build the likelihood function. For each irreducible background contribution, events are divided in three final states ($4\mu$, 4e, and 2e2\mu) and 22 event sub-categories defined in Sect. 6.1. To extract the shape of the $m_{4\ell}$ distribution, expected yields are fitted to empirical functional forms built from a third order Bernstein polynomial. In sub-categories with not enough statistics to perform a fit, the shape is extracted from the inclusive distribution in the corresponding final state.

7.2 Reducible backgrounds

Additional backgrounds to the H boson signal in the $4\ell$ channel arise from processes in which decays of heavy-flavor hadrons, in-flight decays of light mesons within jets, or (for electrons) charged hadrons overlapping with $n^0$ decays are misidentified as leptons. The main processes leading to these backgrounds are Z+jets, t\bar{t}+jets, Z\gamma+jets, WW+jets, and WZ+jets production. We denote these reducible backgrounds as “Z+X” since they are dominated by the Z+jets process. The contribution from the reducible background is estimated with two independent methods, each with dedicated control regions in data. The control regions are defined by the presence of both a lepton pair satisfying all the requirements of a Z1 candidate and two additional opposite sign (OS) or same sign (SS) leptons; the two additional leptons satisfy identification requirements looser than those used in the analysis. These four leptons are then required to pass the analysis ZZ candidate selection. The event yield in the signal region is obtained by weighting the control region events by the lepton misidentification probability $f_e$ ($f_\mu$), defined as the fraction of non-signal electrons (muons) that are identified by the analysis selection criteria. A detailed description of both methods can be found in Ref. [18].

The lepton misidentification rates $f_e$ and $f_\mu$ are measured as a function of $p_T$ and $\eta$ by means of a sample that includes a Z1 candidate consisting of a pair of leptons, both passing the selection requirements used in the analysis, and exactly one additional lepton passing the relaxed selection. Furthermore, the $p_T^{\text{miss}}$ is required to be less than 25 GeV in order to suppress contamination from WZ and t\bar{t} processes.

For the OS method, the mass of the Z1 candidate is required to satisfy the condition $|Z_1 - m_Z| < 7$ GeV in order to reduce the contribution of (asymmetric) photon conversions, which is estimated separately. In the SS method, the contribution of photon conversions to the misidentification rate is estimated with dedicated samples. The predicted yields of the reducible background from the two methods are in agreement within their uncertainties for each final state ($4\mu$, 4e, and 2e2\mu). The final yield used in the analysis is a weighted average of the two independent estimates. To extract the shape of the $m_{4\ell}$ distribution for the reducible background a maximum-likelihood fit is performed in each of the 22 event sub-categories defined in Sect. 6.1. For each sub-category, the expected "Z+X" yields from the OS and SS methods are binned as a function of $m_{4\ell}$ and fitted to empirical functional forms built from Landau distributions [108]. In sub-categories with not enough statistics to perform a fit, the shape is extracted from the inclusive distribution in the corresponding final state.

The dominant systematic uncertainty on the reducible background estimation arises from the difference in the composition of the sample from which the misidentification rate is computed and that of the control regions. It is determined from the MC simulation and is found to be around 30%, depending on the final state. Additional sources of systematic uncertainty arise from the limited number of events in the control regions as well as in the region where the misidentification rates are computed.
8 Signal modeling

In order to generate an accurate signal model, the $p_T$ spectrum of the $H$ boson, $p_T^{H}$, was tuned in the POWHEG simulation of the dominant gluon fusion production mode to better match the predictions from full phase space calculations implemented in the HRES generator [107,109,110].

In order to take advantage of the accuracy of the NNLOPS [111] simulation available for the ggH process, an event reweighting procedure is used. Events originating from the ggH process are subdivided into classes with 0, 1, 2, and $\geq 3$ jets; the jets with $p_T > 30$ GeV are clustered from all stable particles using the anti-$k_T$ algorithm with a distance parameter of 0.4, excluding the decay products of the $H$ boson or associated vector bosons. The weights are obtained as the ratios of the $p_H^T$ distributions from the nnlops and the powheg generators for each event class; the sum of the weights in each sample is normalized to the inclusive cross section.

The signal shape is parametrized by means of a double-sided Crystal Ball function [112] around $m_H \approx 125$ GeV. A Landau function is added in the total probability density function for the non-resonant part of the signal for the case of WH, ZH and $t\bar{t}H$ production modes. The signal shape is parametrized as a function of $m_H$ by performing a simultaneous fit of several mass points for all production modes in the 105 to 140 GeV mass range. Each parameter of the double-sided Crystal Ball function has a linear dependence on $m_H$, for a total of 12 free parameters. An examples of the fit is shown in Fig. 2.

9 Systematic uncertainties

The systematic uncertainties are divided into experimental and theoretical. The main experimental uncertainties originate from the imperfect knowledge of the detector; the dominant sources are the uncertainties in the luminosity measurement, the lepton reconstruction and selection efficiency, the lepton and jet energy scale and resolution, the $b$-tagging efficiency, and the reducible background estimate. The theoretical uncertainties account for the uncertainties in the modeling of the signal and background processes.

Both types of uncertainties can affect the signal selection, cause migrations between the event categories, and affect the signal or background shapes used in the fit. All the uncertainties affecting this analysis are modeled as nuisance parameters (NPs) that are profiled in the maximum likelihood fit described in Sect. 10.

In the combination of the three data-taking periods, all theoretical uncertainties are treated as correlated across these periods. The experimental uncertainties related to reconstruction and selection efficiency, the lepton energy scale and resolution, and the $b$-tagging efficiency are also considered correlated across data-taking periods. Luminosity uncertainty is treated as partially correlated. All other experimental uncertainties are treated as uncorrelated. Correlated sources of uncertainty are assigned the same NP and uncorrelated sources have a dedicated NP in the likelihood fit described in Sect. 10.

The dominant sources of uncertainties and their effect on the analysis are discussed in detail in the following subsections. The impact of a NP on a parameter of interest (POI) is defined as the shift induced on POI when NP is varied by a $\pm 1$ standard deviation from its post-fit value, with all other parameters profiled as usual. The relative impact of the dominant systematic uncertainties on some of the measurements discussed in Sect. 10 is illustrated in Fig. 3.
Fig. 3 The impact of the dominant systematic uncertainties (in percent) on the inclusive signal strength $\mu$ and stage 0 production mode cross section described in Sect. 10. Impacts from different NPs are combined assuming no correlation. Only dominant experimental sources are presented: integrated luminosity uncertainty (Lumi.), lepton reconstruction and selection efficiency, scale and resolution (Leptons), jet energy scale and resolution (Jet), b-tagging efficiency (B-tag), and reducible background estimation uncertainty (Red. bkg). Only dominant theoretical sources are presented: ggH, VBF, and VH cross section theoretical uncertainty scheme (THU), renormalization and factorization scale (QCD), choice of the PDF set (PDF), the branching fraction of $H \rightarrow 4\ell$ ($B$), modeling of hadronization and the underlying event (Hadr), and background modeling (Bkg. mod.). The THU uncertainty is not considered in the stage 0 cross section measurements. The uncertainties are rounded to the nearest 0.5%.
Fig. 4 Four-lepton mass distribution, $m_{4\ell}$, up to 500 GeV with 4 GeV bin size (upper) and in the low-mass range with 2 GeV bin size (lower). Points with error bars represent the data and stacked histograms represent the expected distributions for the signal and background processes. The SM Higgs boson signal with $m_H = 125$ GeV, denoted as $H(125)$, the ZZ and rare electroweak backgrounds are normalized to the SM expectation, the $Z+X$ background to the estimation from data.

9.1 Experimental uncertainties

The integrated luminosities of the 2016, 2017, and 2018 data-taking periods are individually known with uncertainties in the 2.3–2.5% range [41–43], while the total Run 2 (2016–2018) integrated luminosity has an uncertainty of 1.8%, the improvement in precision reflecting the (uncorrelated) time evolution of some systematic effects. The experimental uncertainty on the integrated luminosity measurement affects all final states, both signal and background. Another experimental uncertainty common to all final states is the uncertainty in the lepton reconstruction and selection efficiency. Here selection efficiency includes all the steps from trigger to impact parameter significance and finally identification and isolation requirements. The uncertainty ranges from 1
Table 3 Number of expected background and signal events and number of observed candidates after full analysis selection, for each event category, in the mass range \(105 < m_{4\ell} < 140 \text{ GeV}\) and for an integrated luminosity of 137 fb\(^{-1}\). The yields are given for the different production modes. The uncertainties listed are statistical only. Signal is estimated from MC simulation at \(m_H = 125 \text{ GeV}\), ZZ and rare electroweak backgrounds are also estimated from MC simulation, and Z+X is estimated from data.

| Reconstructed event category | Signal | Background | Expected | Observed |
|-----------------------------|--------|------------|----------|----------|
|                | ggH | VBF | WH | ZH | t\(\bar{t}\)H | bbH | t\(\bar{t}\)H | q\(\bar{q}\) \(\rightarrow\) ZZ | gg \(\rightarrow\) ZZ | EW | Z+X | Signal | Total | |
| Untagged-0j-\(p_T^d\) \([0, 10]\) | 27.7 | 0.09 | 0.03 | 0.03 | 0.00 | 0.15 | 0.00 | 71.5 | 3.06 | 0.01 | 3.21 | 27.9 ± 0.1 | 106 ± 0 | 114 |
| Untagged-0j-\(p_T^d\) \([10, 200]\) | 96.2 | 1.69 | 0.60 | 0.77 | 0.01 | 1.01 | 0.00 | 98.1 | 11.6 | 0.35 | 37.8 | 100 ± 0 | 248 ± 1 | 278 |
| Untagged-1j-\(p_T^d\) \([0, 60]\) | 26.8 | 1.51 | 0.56 | 0.48 | 0.01 | 0.45 | 0.01 | 25.3 | 3.02 | 0.64 | 14.2 | 29.8 ± 0.1 | 72.9 ± 0.4 | 74 |
| Untagged-1j-\(p_T^d\) \([60, 120]\) | 13.5 | 1.31 | 0.51 | 0.41 | 0.02 | 0.11 | 0.01 | 7.81 | 0.82 | 0.62 | 7.95 | 15.9 ± 0.1 | 33.1 ± 0.3 | 20 |
| Untagged-1j-\(p_T^d\) \([120, 200]\) | 3.51 | 0.60 | 0.17 | 0.17 | 0.01 | 0.02 | 0.00 | 1.15 | 0.19 | 0.25 | 1.63 | 4.48 ± 0.05 | 7.69 ± 0.16 | 11 |
| Untagged-2j-\(p_T^d\) \([0, 60]\) | 3.45 | 0.29 | 0.15 | 0.14 | 0.08 | 0.09 | 0.02 | 2.14 | 0.32 | 0.63 | 4.75 | 4.20 ± 0.06 | 12.1 ± 0.2 | 14 |
| Untagged-2j-\(p_T^d\) \([60, 120]\) | 5.26 | 0.56 | 0.24 | 0.19 | 0.12 | 0.04 | 0.03 | 2.19 | 0.30 | 0.72 | 4.14 | 6.43 ± 0.06 | 13.8 ± 0.2 | 15 |
| Untagged-2j-\(p_T^d\) \([120, 200]\) | 3.07 | 0.40 | 0.16 | 0.13 | 0.07 | 0.01 | 0.02 | 0.75 | 0.14 | 0.34 | 1.19 | 3.86 ± 0.05 | 6.28 ± 0.14 | 7 |
| Untagged-\(p_T^d > 200\) | 2.79 | 0.62 | 0.21 | 0.17 | 0.07 | 0.01 | 0.02 | 0.43 | 0.21 | 0.21 | 0.73 | 3.89 ± 0.04 | 5.47 ± 0.11 | 3 |
| Untagged-2j-\(m_{ij} > 350\) | 0.77 | 0.16 | 0.06 | 0.04 | 0.05 | 0.01 | 0.01 | 0.34 | 0.06 | 0.31 | 1.71 | 1.12 ± 0.02 | 3.54 ± 0.14 | 3 |
| VBF-1jet-tagged | 15.5 | 3.29 | 0.22 | 0.16 | 0.00 | 0.13 | 0.01 | 6.85 | 1.53 | 0.20 | 2.44 | 19.3 ± 0.1 | 30.3 ± 0.2 | 27 |
| VBF-2jet-tagged-\(m_{jj} > 350\) | 0.83 | 1.19 | 0.01 | 0.01 | 0.00 | 0.01 | 0.00 | 0.19 | 0.07 | 0.11 | 0.14 | 2.05 ± 0.03 | 2.55 ± 0.05 | 2 |
| VBF-2jet-tagged-\(m_{jj} > 700\) | 0.43 | 1.96 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.07 | 0.05 | 0.12 | 0.03 | 2.40 ± 0.02 | 2.67 ± 0.03 | 1 |
| VBF-3jet-tagged-\(m_{jj} > 350\) | 2.52 | 2.35 | 0.06 | 0.06 | 0.03 | 0.03 | 0.05 | 0.62 | 0.21 | 0.64 | 2.43 | 5.11 ± 0.05 | 9.01 ± 0.17 | 12 |
| VBF-2jet-tagged-\(p_T^d > 200\) | 0.44 | 0.79 | 0.01 | 0.01 | 0.00 | 0.00 | 0.00 | 0.03 | 0.03 | 0.04 | 0.06 | 1.26 ± 0.02 | 1.42 ± 0.03 | 0 |
| VBF-rest | 2.48 | 0.94 | 0.13 | 0.09 | 0.04 | 0.04 | 0.01 | 0.98 | 0.20 | 0.39 | 2.18 | 3.74 ± 0.05 | 7.49 ± 0.17 | 5 |
| VH-hadronic-tagged-\(m_{jj} > 60, 120\) | 4.11 | 0.25 | 1.09 | 0.96 | 0.13 | 0.06 | 0.02 | 1.69 | 0.22 | 0.52 | 2.93 | 6.62 ± 0.06 | 12.0 ± 0.2 | 12 |
| VH-rest | 0.57 | 0.03 | 0.09 | 0.06 | 0.03 | 0.01 | 0.00 | 0.16 | 0.02 | 0.06 | 0.33 | 0.79 ± 0.02 | 1.36 ± 0.06 | 0 |
| VH-leptonic-tagged-\(p_T^d [0, 150]\) | 0.33 | 0.04 | 0.85 | 0.26 | 0.10 | 0.03 | 0.03 | 2.16 | 0.36 | 0.19 | 1.11 | 1.64 ± 0.02 | 5.47 ± 0.13 | 10 |
| VH-leptonic-tagged-\(p_T^d > 150\) | 0.02 | 0.01 | 0.21 | 0.06 | 0.04 | 0.00 | 0.01 | 0.05 | 0.01 | 0.03 | 0.08 | 0.35 ± 0.01 | 0.52 ± 0.03 | 0 |
| t\(\bar{t}\)H-leptonic-tagged | 0.02 | 0.01 | 0.02 | 0.02 | 0.68 | 0.00 | 0.03 | 0.08 | 0.01 | 0.23 | 0.21 | 0.79 ± 0.01 | 1.32 ± 0.07 | 0 |
| t\(\bar{t}\)H-hadronic-tagged | 0.18 | 0.05 | 0.03 | 0.05 | 0.86 | 0.01 | 0.03 | 0.03 | 0.01 | 0.82 | 1.06 | 1.22 ± 0.01 | 3.15 ± 0.14 | 2 |
Fig. 6  Distributions of the expected and observed number of events for the reconstructed event categories in the mass region $105 < m_{4\ell} < 140$ GeV. Points with error bars represent the data and stacked histograms represent the expected numbers of the signal and background events. The yields of the different H boson production mechanisms with $m_H = 125$ GeV, denoted as $H(125)$, and those of the $ZZ$ and rare electroweak backgrounds are normalized to the SM expectations, while the $Z+X$ background yield is normalized to the estimate from the data to 2.3% in the $4\mu$ channel and from 11 to 15.5% in the $4e$ channel. While for muon efficiency measurements in the low $p_T$ regions we rely on low mass di-muon resonances, the electron efficiency measurement relies solely on the Z boson resonance, resulting in a higher uncertainty in the low $p_T$ region.

Lepton momentum scale and resolution uncertainties are estimated from dedicated studies on the $Z \rightarrow \ell^+\ell^-$ mass distribution in data and simulation. Events are classified according to the $p_T$ and $\eta$ of one of the two leptons, determined randomly, and integrated over the other. The dilepton mass distributions are then fit by a Breit–Wigner parameterization convolved with the double-sided Crystal Ball function described in Sect. 8. The scale uncertainty is found to be 0.04% in the $4\mu$ channel and 0.3% in the $4e$ channel, while the resolution uncertainty is 20% for both channels. In both cases full correlation between the leptons in the event is assumed. Both scale and resolution uncertainties alter the signal shape by allowing the corresponding parameters of the double-sided Crystal Ball function to vary. The impact is found to be non-negligible only in the case of fiducial cross section measurements.

The effects of the jet energy corrections are studied in a similar manner. While jet energy scale and smearing do not alter signal selection efficiency, they cause event migrations between the categories. They can also alter the shape of the discriminants, but the effect on the shape is negligible. The uncertainty in the jet energy scale ranges from 1% in the high jet $p_T$ range and increases up to 5% in the low jet $p_T$ range. The uncertainty in jet energy resolution ranges from 1 to 2%. A detailed description of the determination of the jet energy scale and smearing uncertainties can be found in [113]. The effect on the analysis is studied in detail by propagating the uncertainties and estimating the effect on event migration in each of the 22 sub-categories. Their impact on the inclusive measurements is found to be negligible. However, the impact is significant in measurements of the VBF and VH production modes and differential cross section measurements as a function of jet kinematics, where it is one of the leading sources of uncertainty.
Fig. 7 Distribution of the $Z_1$ (upper left) and $Z_2$ (upper right) reconstructed masses in the $118 < m_{4\ell} < 130$ GeV mass region and their 2D distribution (lower) in the $105 < m_{4\ell} < 140$ GeV mass region. The stacked histograms and the red and blue scales represent expected distributions of the signal and background processes and the points represent the data. The yields of the different H boson production mechanisms with $m_H = 125$ GeV, denoted as H(125), and those of the ZZ and rare electroweak backgrounds are normalized to the SM expectations, while the Z+X background yield is normalized to the estimate from the data

The uncertainty in the b-tagging efficiency is found to be 1\% in the high jet $p_T$ range and increases up to 3\% in the low jet $p_T$ range. The impact from the category migration is found to be negligible in all categories.

Finally, experimental uncertainties in the reducible background estimation, described in Sect. 7.2, originating from the background composition and misidentification rate uncertainties vary between 30 and 45\% depending on the final state and category. However, the impact of this uncertainty on the measurements is found to be negligible.

Other sources of experimental uncertainties are also studied but their impact is negligible compared to the sources described above.

9.2 Theoretical uncertainties

Theoretical uncertainties that affect both the signal and background estimation include those related to the renormalization and factorization scales, and the choice of the PDF set. The uncertainty from the renormalization and factorization scales is determined by varying these scales between 0.5 and 2 times their nominal value, while keeping their ratio between 0.5 and 2. The uncertainty due to the PDF set is determined following the PDF4LHC recommendations by taking the root mean square of the variation of the results when using different replicas of the default NNPDF set \([114,115]\). The uncertainties just described have an effect both on the signal and background yields, as well as on the migration of events between the categories. An additional 10\% uncertainty in the $K$ factor used for the $gg \rightarrow ZZ$ prediction is applied as described in Sect. 7.1. A systematic uncertainty of 2\% \([32]\) in the branching fraction of $H \rightarrow 4\ell$ only affects the signal yield.

Theoretical uncertainties that affect the predictions of the STXS production bins are described in Ref. \([32]\). From here
Fig. 8 Distribution of categorization discriminants in the mass region $118 < m_{4\ell} < 130$ GeV: $D_{VBF}^{2\ell}$ (upper), $D_{VBF}^{1\ell}$ (center), $D_{VH}^{2\ell}$ (lower) = max($D_{WH}^{2\ell}, D_{ZH}^{2\ell}$). Points with error bars represent the data and stacked histograms represent expected distributions of the signal and background processes. The SM Higgs boson signal with $m_{H} = 125$ GeV, denoted as H(125), is compared with the expectations for signal and background processes. The SM H boson signal is separated into two components: the production mode which is targeted by the specific discriminant, and other production modes, where the gluon fusion process dominates.

10 Results

The reconstructed four-lepton invariant mass distribution is shown in Fig. 4 for the 4e, 4$\mu$, and 2e2$\mu$ events together, and is compared with the expectations for signal and background processes. The error bars on the data points correspond to the intervals at 68% confidence level (CL) [116]. The observed distribution agrees with the expectation within the statistical uncertainties over the whole spectrum.

The reconstructed four-lepton invariant mass distribution is shown in Fig. 5 for the three 4$\ell$ final states and is compared with the expectations from signal and background processes.
Fig. 9 Distribution of three different kinematic discriminants versus $m_{4\ell}$: $\mathcal{D}^{\text{bkg}}_{\text{kin}}$ (upper), $\mathcal{D}^{\text{VBF+dec}}_{\text{bkg}}$ (middle) and $\mathcal{D}^{\text{VH+dec}}_{\text{bkg}}$ (lower) shown in the mass region $105 < m_{4\ell} < 140$ GeV. The blue scale represents the expected total number of ZZ, rare electroweak, and Z+X background events. The red scale represents the number of expected SM H boson signal events for $m_{H} = 125$ GeV. The points show the data from the categories listed in the legend.
Fig. 10 Distribution of kinematic discriminants in the mass region $118 < m_{4\ell} < 130$ GeV: (uppper) $D_{\text{kin}}^{bkg}$, (center) $D_{\text{VBF}}^{+\text{dec}}$, (lower) $D_{\text{VH}}^{+\text{dec}}$. Points with error bars represent the data and stacked histograms represent expected distributions of the signal and background processes. The yields of the different H boson production mechanisms with $m_H = 125$ GeV, denoted as $H(125)$, and those of the ZZ and rare electroweak backgrounds are normalized to the SM expectations, while the Z+X background yield is normalized to the estimate from the data. In the center and lower figures the SM H boson signal is separated into two components: the production mode which is targeted by the specific discriminant, and other production modes, where the gluon fusion process dominates.

The number of candidates observed in the data and the expected yields for 137 fb$^{-1}$, for the backgrounds and H boson signal after the full event selection, are given in Table 3 for each of the 22 reconstructed event categories (described in Sect. 6.2) for the $105 < m_{4\ell} < 140$ GeV mass window around the Higgs boson peak. Fig. 6 shows the number of expected and observed events for each of the categories.

The reconstructed invariant masses of the $Z_1$ and $Z_2$ dilepton systems are shown in Fig. 7 for $118 < m_{4\ell} < 130$ GeV, together with their 2D distribution in the $105 < m_{4\ell} < 140$ GeV mass region. The distribution of the discriminants used for event categorization along with the corresponding working point values are shown in Fig. 8.

The results presented in Sects. 10.1 and 10.2 are extracted with a two-dimensional likelihood fit that relies on two variables, the four-lepton invariant mass $m_{4\ell}$ and the matrix ele-
is performed in the 105 measurements are extracted with a one-dimensional likelihood function. Fig. 12 indicates the best fit value, and the diamond represents the expected range studied. Negative POIs would imply negative signal strength modifiers and a negative probability density function (pdf). We define a two-dimensional pdf as the product of two one-dimensional pdfs:

\[ f(m_{4\ell}, D) = \mathcal{P}(m_{4\ell}) \mathcal{P}(D|m_{4\ell}). \]  

(6)

The first term, \( \mathcal{P}(m_{4\ell}) \), is the un unbinned analytical shape described in Sect. 8 for signals and Sect. 7 for backgrounds. The second term, \( \mathcal{P}(D|m_{4\ell}) \), is a binned template of \( D \) that is conditional to \( m_{4\ell} \). This is achieved by creating a two-dimensional template of \( m_{4\ell} \) vs. \( D \) and normalizing it to 1 for each bin of \( m_{4\ell} \).

In almost all sub-categories we use a decay-only kinematic discriminant (\( D = \mathcal{D}^{\text{kin}} \)) to separate the H boson signal from the background as defined in Eq. (3). Conversely, in the sub-categories of the VBF-2jet-tagged, the \( D = \mathcal{D}^{\text{VBF+dec}} \) discriminant (defined in Eq. (4)) is used, which is sensitive to the VBF production mechanism. Similarly, in two sub-categories of the VH-hadronic-tagged category, the \( D = \mathcal{D}^{\text{VH+dec}} \) discriminant (defined in Eq. (5)) is used.

The ggH, VBF, WH, ZH and tH samples are used to build different signal templates for each of the nineteen STXS production bins described in Sect. 6.1. Irreducible background templates are built starting from q\( \bar{q} \rightarrow ZZ \) and gg \( \rightarrow ZZ \) samples. Finally, reducible background templates are built using data driven methods described in Sect. 7.2. Following the described procedure, \( \mathcal{P}(D|m_{4\ell}) \) templates are obtained for the twenty-two event categories and the three final states (4\( \mu \), 4e, 2e2\( \mu \)).

The unbinned likelihood function, \( \mathcal{L}(\hat{\mu}) \), is defined as the product over \( N \) observed events:

\[ \mathcal{L}(\hat{\mu}) = \prod_{i=1}^{19} \left( \sum_{\mu_{i}} S_{i}^{jk} f_{S}^{ijk}(m_{4\ell}, D) + B_{i}^{jk} f_{B}^{ijk}(m_{4\ell}, D) \right) e^{-\sum_{\mu_{i}} S_{i}^{jk} + B_{i}^{jk}}, \]  

(7)

where \( \mu_{i} \) is the signal strength modifier for the production bin \( i \), \( S_{i}^{jk} \) are the predicted SM rates of events in the production bin \( i \) that are observed in the reconstructed event category \( j \) and final state \( k \), \( B_{i}^{jk} \) are the predicted background rates in the reconstructed event category \( j \) and final state \( k \), \( f_{S}^{ijk}(m_{4\ell}, D) \) and \( f_{B}^{ijk}(m_{4\ell}, D) \) are the probability density functions of the signal and background, respectively.

### Table 4

| Expected          | Observed          |
|-------------------|-------------------|
| \( \mu_{tH,H} \)  | \( 1.00^{+1.23}_{-0.73} \) (stat)\(+0.51_{-0.06} \) (syst) | \( 0.17^{+0.85}_{-0.74} \) (stat)\(+0.42_{-0.05} \) (syst) |
| \( \mu_{WH} \)   | \( 1.00^{+1.83}_{-1.06} \) (stat)\(+0.75_{-0.44} \) (syst) | \( 1.66^{+1.02}_{-0.56} \) (stat)\(+0.85_{-0.36} \) (syst) |
| \( \mu_{ZH} \)   | \( 1.00^{+4.79}_{-1.06} \) (stat)\(+6.76_{-0.00} \) (syst) | \( 0.00^{+1.38}_{-0.00} \) (stat)\(+3.24_{-0.00} \) (syst) |
| \( \mu_{VBF} \)  | \( 1.00^{+0.53}_{-0.42} \) (stat)\(+0.18_{-0.12} \) (syst) | \( 0.48^{+0.46}_{-0.37} \) (stat)\(+0.14_{-0.10} \) (syst) |
| \( \mu_{tH,b\phi H} \) | \( 1.00 \pm 0.10 \) (stat)\(+0.12_{-0.10} \) (syst) | \( 0.99 \pm 0.09 \) (stat)\(+0.14_{-0.09} \) (syst) |
| \( \mu \)        | \( 1.00^{+0.08}_{-0.06} \) (stat)\(+0.10_{-0.08} \) (syst) | \( 0.94 \pm 0.07 \) (stat)\(+0.09_{-0.08} \) (syst) |
Fig. 13 The measured product of cross section times branching fraction for $H \rightarrow ZZ$ decay ($\sigma B_{\text{obs}}$) and the SM predictions ($\sigma B_{\text{SM}}$) for the stage 0 STXS production bins and the inclusive measurement at $m_H = 125.38$ GeV. Points with error bars represent measured values and black dashed lines with gray uncertainty bands represent the SM predictions. In the bottom panel ratios of the measured cross sections and the SM predictions are shown along with the uncertainties for each of the bins and the inclusive measurement.

Identification of the lepton signatures are the pdfs for the signal, and $f_{jk}^{B}(m_{4\ell}, D)$ the pdfs for the background.

The correlation of the kinematic discriminants $D_{\text{bkg}}^{\text{kin}}$, $D_{\text{bkg}}^{\text{VBF+dec}}$, and $D_{\text{bkg}}^{\text{VH+dec}}$ with the four-lepton invariant mass is shown in Fig. 9 for the mass interval $105 < m_{4\ell} < 140$ GeV. Their distributions for the mass interval $118 < m_{4\ell} < 130$ GeV are shown in Fig. 10.

10.1 Signal strength modifier

A simultaneous fit to all categories is performed to extract the signal strength modifier, defined as the ratio of the observed H boson yield in the $H \rightarrow 4\ell$ decay channel to the standard model expectation.

The combined measurement of the inclusive signal strength modifier is measured to be $\mu = 0.94^{+0.12}_{-0.11}$ or $\mu = 0.94 \pm 0.07 \text{ (stat)}^{+0.07}_{-0.06} \text{ (theo)}^{+0.06}_{-0.05} \text{ (exp)}$ at a fixed mass value $m_H = 125.38$ GeV, which is the current most precise measurement of the H boson mass published by the CMS Collaboration [119]. In all subsequent fits, $m_H$ is fixed to this value. The dominant experimental sources of systematic uncertainty are the uncertainties in the lepton identification efficiencies and luminosity measurement, while the dominant theoretical source is the uncertainty in the total gluon fusion cross section. The contributions to the total uncertainty from experimental and theoretical sources are found to be similar in magnitude. The signal strength modifiers are further studied in terms of the five main SM Higgs boson production mechanisms, namely ggH, VBF, ZH, WH, and t\bar{t}H. The contributions of the b\bar{b}H and tH production modes are also taken into account. The relative normalizations of the b\bar{b}H and the gluon fusion contributions are kept fixed in the fit, and so are the t\bar{t}H and tH ones. The results are shown in Fig. 11 for the observed and expected profile likelihood scans of the inclusive signal strength modifier and those for the signal strength modifiers of the five main SM Higgs boson production mechanisms. The corresponding numerical values, including the decomposition of the uncertainties into statistical and systematic components, as well as the expected uncertainties, are given in Table 4.

The dependence of the measured signal strengths on the profiling of $m_H$ is checked and found to have a small impact both on the inclusive results and those in terms of the five main H boson production mechanisms, well within the measurement uncertainties. The best fit signal value changes at most by 4% and the profiled value of the mass is found to be $m_H = 125.09^{+0.15}_{-0.14}$ (stat) GeV. It is important to note here that the precise determination of $m_H$ and the systematic uncer-
Fig. 14 The measured cross sections \((σ\beta)_{\text{obs}}\) and the SM predictions \((σ\beta)_{\text{SM}}\) for \(H \rightarrow ZZ\) decay and the merged stage 1.2 STXS production bins at \(m_H = 125.38\) GeV. Points with error bars represent measured values and black dashed lines with gray uncertainty bands represent the SM predictions. In the bottom panel ratios of the measured cross sections and the SM predictions are shown with corresponding uncertainties for each of the bins.

Table 5 Best fit values and ±1 standard deviation uncertainties for the measured cross sections \((σ\beta)_{\text{obs}}\), the SM predictions \((σ\beta)_{\text{SM}}\), and their ratio for the stage 0 STXS production bins at \(m_H = 125.38\) GeV for \(H \rightarrow ZZ\) decay.

| Production Channel | \((σ\beta)_{\text{obs}}\) (fb) | \((σ\beta)_{\text{SM}}\) (fb) | \((σ\beta)_{\text{obs}}/(σ\beta)_{\text{SM}}\) |
|-------------------|----------------|----------------|--------------|
| \(t\bar{t}H\)     | 3.16 ± 1.16   | 15.9 ± 1.4    | 0.16 ± 0.36  |
| \(\nu\nuH\)       | 4.2 ± 3.4     | 25.9 ± 0.6    | 1.56 ± 0.19  |
| \(qgH\)           | 8.6 ± 5.3     | 122 ± 6      | 0.50 ± 0.44  |
| \(ggH\)           | 12.3 ± 13.5   | 1192 ± 95    | 1.02 ± 0.11  |
| Inclusive         | 13.8 ± 1.30   | 1369 ± 164   | 0.96 ± 0.10  |

The 68 and 95% CL contours in the \((μ_f, μ_V)\) plane are shown in Fig. 12 and the SM predictions lie within the 68% CL regions of this measurement.

10.2 Simplified template cross section

The results for the H boson product of cross section times branching fraction for \(H \rightarrow ZZ\) decay, \((σ\beta)_{\text{obs}}\), and comparisons with the SM expectation, \((σ\beta)_{\text{SM}}\), for the stages of production bins defined in Sect. 6.1, are shown in Fig. 13 for the stage 0 and in Fig. 14 for the merged stage 1.2. The corresponding numerical values are given in Tables 5 and 6.

As discussed, the set of THU uncertainties described in Sect. 9.2 is not considered for the STXS measurements: THU uncertainties that enter its measurement are beyond the scope of this analysis.

Two signal strength modifiers, \(μ_f \equiv μ_{gH, tH, bH, tH} \) and \(μ_V \equiv μ_{VBF, VH} \), are introduced for the fermion and vector-boson induced contributions to the expected SM cross section. A two-parameter fit is performed simultaneously to the events reconstructed in all categories, leading to \(μ_f = 0.96^{+0.14}_{-0.13}\) and \(μ_V = 0.82^{+0.36}_{-0.31}\). The expected values for \(m_H = 125.38\) GeV are \(μ_f = 1.00^{+0.15}_{-0.13}\) and \(μ_V = 1.00^{+0.39}_{-0.33}\). The 68 and 95% CL contours in the \((μ_f, μ_V)\) plane are shown in Fig. 12 and the SM predictions lie within the 68% CL regions of this measurement.
uncertainties are model dependent and should be only considered in the interpretation of the results. Therefore, the THU uncertainties are included in the SM predictions of the cross section. The correlation matrices are shown in Fig. 15. The dominant experimental sources of systematic uncertainty are the same as for the signal strength modifiers measurement, while the dominant theoretical source is the uncertainty in the category migration for the ggH process.

10.3 Fiducial cross section

In this section the cross section measurement for the process \( pp \rightarrow H \rightarrow 4\ell \) within a fiducial volume that closely matches the reconstruction level selection is presented. In particular, the integrated fiducial cross section is measured as well as differential cross sections as a function of the transverse momentum of the H boson \( p_T^H \), its rapidity \(|y^H|\), the number of associated jets \( N_j^Q\), and the transverse momentum of the leading jet \( p_T^1 \). These measurements are largely independent of the assumptions on the relative fractions and kinematic distributions of the individual production modes. The definition of the fiducial volume is based on generator-level quantities and is identical to that in Ref. [18]. In order to reduce the experimental uncertainties, only jets with \( p_T^j > 30 \) GeV and \(|p_T^j| < 2.5\) are considered for the differential cross sections as a function of jet observables. An increase in model dependence compared to Ref. [25] is observed when using the ZZ candidate selection at reconstruction level where the candidate with the best \( D_{\text{bkg}}^\text{kin} \) discriminant value is chosen. Therefore, the fiducial cross section measurement is performed using the event selection algorithm in Ref. [25]. Specifically, the \( Z\ell \) candidate is chosen to be the one with \( m(Z\ell) \) closest to the nominal Z boson mass, and in cases where multiple \( Z\ell \) candidates satisfy all criteria, the pair of leptons with the largest sum of the transverse momenta magnitudes is chosen. The full fiducial volume definition is detailed in Table 7 and the acceptance for various SM production modes is given in Table 8.

A maximum likelihood fit of the signal and background parameterizations to the observed 4\ell mass distribution, \( N_{\text{obs}}(m_{4\ell}) \), is performed to extract the integrated fiducial cross section for the process \( pp \rightarrow H \rightarrow 4\ell \left(\sigma_{\text{fid}}\right) \). The fit is carried out inclusively (i.e., without any event categorization) and does not use the \( D_{\text{bkg}}^\text{kin} \) observable in order to minimize the model dependence. The fit is performed simultaneously in all final states and assumes a H boson mass \( m_H = 125.38 \) GeV, while the branching fractions of the H boson to different final states \((4e, 4\mu, 2e2\mu)\) are free parameters in the fit. The systematic uncertainties described in Sect. 9 are included in the form of NPs and the results are obtained using an asymptotic approach [118] with a test statistic based on the profile likelihood ratio [117]. This procedure accounts for the unfolding of detector effects from the observed distributions and is the same as in Refs. [25, 120].
Fig. 15  Correlation matrices between the measured cross sections for the stage 0 (upper) and the merged stage 1.2 (lower) for $H \rightarrow ZZ$ decay.
Table 7  Summary of requirements used in the definition of the fiducial phase space for the H → 4ℓ cross section measurements

Requirements for the H → 4ℓ fiducial phase space

Lepton kinematics and isolation

| Event topology | Requirement |
|----------------|-------------|
| Inv. mass of the Z1 candidate | 40 < mZ1 < 120 GeV |
| Inv. mass of the Z2 candidate | 12 < mZ2 < 120 GeV |
| Distance between selected four leptons | ΔR(ℓi, ℓj) > 0.02 for any i ≠ j |
| Inv. mass of any opposite sign lepton pair | ml+ℓ− > 4 GeV |
| Inv. mass of the selected four leptons | 105 < m4ℓ < 140 GeV |

Event topology

Existence of at least two same-flavor OS lepton pairs, where leptons satisfy criteria above

| Signal process | Afid | ϵ | fnonfid | (1 + fnonfid)ϵ |
|----------------|------|---|--------|--------------|
| ggH (POWHEG)  | 0.402 ± 0.001 | 0.598 ± 0.002 | 0.054 ± 0.001 | 0.631 ± 0.002 |
| VBF            | 0.445 ± 0.002 | 0.615 ± 0.002 | 0.043 ± 0.001 | 0.641 ± 0.003 |
| WH             | 0.329 ± 0.002 | 0.604 ± 0.003 | 0.078 ± 0.002 | 0.651 ± 0.004 |
| ZH             | 0.340 ± 0.003 | 0.613 ± 0.005 | 0.082 ± 0.004 | 0.663 ± 0.006 |
| tH             | 0.315 ± 0.004 | 0.588 ± 0.007 | 0.181 ± 0.009 | 0.694 ± 0.010 |

The number of expected events in each final state f and in each bin i of a given observable is expressed as a function of m4ℓ as:

\[ N_{\text{exp}}^{f,i}(m_{4\ell}) = N_{\text{fid}}^{f,i}(m_{4\ell}) + N_{\text{non fid}}^{f,i}(m_{4\ell}) + N_{\text{nonres}}^{f,i}(m_{4\ell}) + \epsilon \sigma_{\text{fid}} f_{\text{res}}(m_{4\ell}) \]

The shape of the resonant signal contribution, \( P_{\text{res}}(m_{4\ell}) \), is described by a double-sided Crystal Ball function as discussed in Sect. 8, and the normalization is used to extract the fiducial cross section. The non-resonant signal function, \( P_{\text{nonres}}(m_{4\ell}) \), is determined by the WH, ZH, and tH contributions where one of the leptons from the H boson decay is lost or not selected. It is modeled by a Landau distribution with shape parameters constrained in the fit to be within a range determined from simulation. This contribution is referred to as the “combinatorial signal” and is treated as a background in this measurement.

The quantity \( \epsilon_{i,j}^f \) represents the detector response matrix that maps the number of expected events in bin j of a given observable at the fiducial level to the number of expected events in bin i at the reconstruction level. This response matrix is determined using simulated signal samples and includes corrections for residual differences between data and simulation. In the case of the integrated fiducial cross section measurement, the response matrices become single numbers, which are listed in Table 8 for different SM production mechanism.

An additional resonant contribution arises from events which are accepted but do not originate from the fiducial phase space. These events are due to detector effects that cause differences between the quantities used for the fiducial phase space definition and the corresponding quantities at the reconstruction level. This contribution is treated as background and is referred to as the “non-fiducial signal” contribution. A simulated sample is used to verify that the shape of the distribution for these events is identical to that of the fiducial signal, and its normalization is fixed to the corresponding fraction of the fiducial signal. The value of
Fig. 16 The measured inclusive fiducial cross section in different final states (upper) and integrated as a function of $\sqrt{s}$ (lower). The acceptance is calculated using POWHEG at $\sqrt{s} = 13$ TeV and HRES [107,109] at $\sqrt{s} = 7$ and 8 TeV, and the total gluon fusion cross section and uncertainty are taken from Ref. [58]. The fiducial volume for $\sqrt{s} = 6$–9 TeV uses the lepton isolation definition from Ref. [25] and the SM predictions and measurements are calculated at $m_H = 125.38$ GeV.

The measured fiducial cross sections as a function of the center-of-mass energy are shown in Fig. 16. The corresponding numerical values, including the decomposition of the uncertainties into statistical and systematic components, and the corresponding expected uncertainties, are given in Table 9.

For all the fiducial measurements the dominant systematic uncertainties are those on the lepton identification efficiencies and luminosity measurement, while the theoretical uncertainties are smaller. In order to assess the model dependence of the measurement, the unfolding procedure is repeated using different response matrices created by varying the relative fraction of each SM production mode within its experimental constraints. The uncertainty is negligible with respect to the experimental systematic uncertainties.

11 Summary

Several measurements of the Higgs boson production in the four-lepton final state at $\sqrt{s} = 13$ TeV have been presented, using data samples corresponding to an integrated luminosity of 137 fb$^{-1}$. Thanks to a large signal-to-background ratio and the complete reconstruction of the final state decay products, this channel enables a detailed study of the Higgs boson production properties. The measured signal strength modifier is $\mu = 0.94 \pm 0.07$ (stat)$^{+0.07}_{-0.06}$ (theo)$^{+0.06}_{-0.05}$ (exp) and the integrated fiducial cross section is measured to be $\sigma_{\text{fid}} = 2.84^{+0.23}_{-0.22}$ (stat)$^{+0.26}_{-0.21}$ (syst) fb with a standard model prediction of $2.84 \pm 0.15$ fb for the same fiducial region. The signal strength modifiers for the main Higgs boson production modes are also reported. A new set of measurements, designed to quantify the different Higgs boson production processes in specific kinematical regions of phase space, have also been presented. The differential cross sections as a function of the transverse momentum and rapidity of the Higgs boson, the number of associated jets, and the transverse momentum of the leading associated jet are determined. All results are consistent, within their uncertainties, with the expectations for the standard model Higgs boson.
Table 9 The measured inclusive fiducial cross section and ±1 standard deviation uncertainties for different final states and data-taking periods at $m_H = 125.38$ GeV. The statistical and systematic uncertainties are given separately for the inclusive measurements.

| Year      | $2e2\mu$ (fb) | $4\mu$ (fb) | $4e$ (fb) | Inclusive (fb) |
|-----------|---------------|-------------|-----------|---------------|
| 2016      | 1.22^{+0.38}_{-0.30} | 0.89^{+0.22}_{-0.19} | 1.07^{+0.44}_{-0.33} | 3.19^{+0.68}_{-0.56} = 3.19^{+0.48}_{-0.45} (stat)^{+0.34}_{-0.32} (syst) |
| 2017      | 1.64^{+0.41}_{-0.35} | 0.82^{+0.21}_{-0.18} | 0.56^{+0.29}_{-0.22} | 3.01^{+0.60}_{-0.50} = 3.01^{+0.44}_{-0.41} (stat)^{+0.44}_{-0.41} (syst) |
| 2018      | 1.17^{+0.27}_{-0.24} | 0.66^{+0.15}_{-0.13} | 0.73^{+0.24}_{-0.20} | 2.57^{+0.42}_{-0.38} = 2.57^{+0.33}_{-0.31} (stat)^{+0.27}_{-0.27} (syst) |
| 2016–2018 | 1.31^{+0.20}_{-0.19} | 0.78^{+0.10}_{-0.10} | 0.76^{+0.16}_{-0.16} | 2.84^{+0.34}_{-0.31} = 2.84^{+0.33}_{-0.32} (stat)^{+0.28}_{-0.28} (syst) |

![Fig. 17](https://example.com/fig17.png)

**Fig. 17** Differential cross sections as a function of $p_T^H$ (upper) and $|y^H|$ (lower). The acceptance and theoretical uncertainties in the differential bins are calculated using POWHEG. The sub-dominant component of the signal (VBF + VH + (t)H) is denoted as XH.

Table 10 The measured differential fiducial cross section and ±1 standard deviation uncertainties for the $p_T^H$ observable at $m_H = 125.38$ GeV. The breakdown of the total uncertainty (unc.) into statistical and systematic components is given.

| Bin range (GeV) | $d\sigma_{\text{fid}}$ (fb) | unc. (fb) | stat (fb) | syst (fb) |
|-----------------|-----------------------------|-----------|-----------|-----------|
| 0–10            | 0.32                        | +0.11     | +0.10     | +0.04     |
| 10–20           | 0.67                        | +0.14     | +0.13     | +0.06     |
| 20–30           | 0.41                        | +0.12     | +0.11     | +0.04     |
| 30–45           | 0.51                        | +0.12     | +0.11     | +0.04     |
| 45–80           | 0.45                        | +0.10     | +0.10     | +0.04     |
| 80–120          | 0.30                        | +0.08     | +0.07     | +0.02     |
| 120–200         | 0.19                        | +0.06     | +0.06     | +0.01     |
| 200–13000       | 0.03                        | +0.02     | +0.02     | +0.00     |

Table 11 The measured differential fiducial cross section and ±1 standard deviation uncertainties for the $|y^H|$ observable at $m_H = 125.38$ GeV. The breakdown of the total uncertainty (unc.) into statistical and systematic components is given.

| Bin range | $d\sigma_{\text{fid}}$ (fb) | unc. (fb) | stat (fb) | syst (fb) |
|-----------|-----------------------------|-----------|-----------|-----------|
| 0.0–0.15  | 0.41                        | +0.10     | +0.09     | +0.05     |
| 0.15–0.3  | 0.36                        | +0.08     | +0.07     | +0.03     |
| 0.3–0.6   | 0.62                        | +0.13     | +0.11     | +0.07     |
| 0.6–0.9   | 0.57                        | +0.12     | +0.10     | +0.06     |
| 0.9–1.2   | 0.36                        | +0.10     | +0.09     | +0.05     |
| 1.2–2.5   | 0.64                        | +0.15     | +0.13     | +0.08     |

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Differential cross sections as a function of the number of associated jets (upper), and \( p_T \) of the leading jet (lower). The acceptance and theoretical uncertainties in the differential bins are calculated using POWHEG. The sub-dominant component of the signal (VBF + VH + tH) is denoted as XH.

Table 12 The measured differential fiducial cross section and \( \pm 1 \) standard deviation uncertainties for the \( N_j \) observable at \( m_{t\bar{t}} = 125.38 \) GeV. The breakdown of the total uncertainty (unc.) into statistical and systematic components is given.

| Bin range | \( d\sigma_{\text{fid}} \) (fb) | unc. (stat) | (syst) |
|-----------|-------------------------------|-------------|--------|
| 0         | 2.00                         | +0.29       | +0.21  |
| 1         | 0.64                         | +0.15       | +0.14  |
| 2         | 0.23                         | +0.09       | +0.09  |
| 3         | 0.03                         | +0.05       | +0.05  |
| \( \geq 4 \) | 0.00                         | +0.03       | +0.03  |

Table 13 The measured differential fiducial cross section and \( \pm 1 \) standard deviation uncertainties for the \( p_T \) observable at \( m_{t\bar{t}} = 125.38 \) GeV. The breakdown of the total uncertainty (unc.) into statistical and systematic components is given.

| Bin range (GeV) | \( d\sigma_{\text{fid}} \) (fb) | unc. (stat) | (syst) |
|----------------|-------------------------------|-------------|--------|
| 30–55          | 0.52                         | +0.16       | +0.15  |
| 55–95          | 0.21                         | +0.10       | +0.10  |
| 95–200         | 0.16                         | +0.07       | +0.06  |
| 200–1300       | 0.04                         | +0.03       | +0.03  |

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Declaration

Conflict of interest The authors declare that they have no conflict of interest.

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8: Also at Department of Physics, Tsinghua University, Beijing, China, Beijing, China
9: Also at Nanjing Normal University Department of Physics, Nanjing, China
10: Now at The University of Iowa, Iowa City, USA
11: Also at Institute for Theoretical and Experimental Physics named by A.I. Alikhanov of NRC ‘Kurchatov Institute’, Moscow, Russia
12: Also at Joint Institute for Nuclear Research, Dubna, Russia
13: Also at Ain Shams University, Cairo, Egypt
14: Also at Zewail City of Science and Technology, Zewail, Egypt
15: Also at British University in Egypt, Cairo, Egypt
16: Also at Purdue University, West Lafayette, USA
17: Also at Université de Haute Alsace, Mulhouse, France
18: Also at Erzincan Binali Yıldırım University, Erzincan, Turkey
19: Also at CERN European Organization for Nuclear Research, Geneva, Switzerland
20: Also at III. Physikalisches Institut A, RWTH Aachen University, Aachen, Germany
21: Also at University of Hamburg, Hamburg, Germany
22: Also at Department of Physics, Isfahan University of Technology, Isfahan, Iran
23: Also at Brandenburg University of Technology, Cottbus, Germany
24: Also at Skobeltsyn Institute of Nuclear Physics, Lomonosov Moscow State University, Moscow, Russia
25: Also at Physics Department, Faculty of Science, Assiut University, Assiut, Egypt
26: Also at Eszterhazy Karoly University, Karoly Robert Campus, Gyongyos, Hungary
27: Also at Institute of Physics, University of Debrecen, Debrecen, Hungary
28: Also at Institute of Nuclear Research ATOMKI, Debrecen, Hungary
29: Also at MTA-ELTE Lendület CMS Particle and Nuclear Physics Group, Eötvös Loránd University, Budapest, Hungary
30: Also at Wigner Research Centre for Physics, Budapest, Hungary
31: Also at IIT Bhubaneswar, Bhubaneswar, India
32: Also at Institute of Physics, Bhubaneswar, India
33: Also at G.H.G. Khalsa College, Punjab, India
34: Also at Shoolini University, Solan, India
35: Also at University of Hyderabad, Hyderabad, India
36: Also at University of Visva-Bharati, Santiniketan, India
37: Also at Indian Institute of Technology (IIT), Mumbai, India
38: Also at Deutsches Elektronen-Synchrotron, Hamburg, Germany
39: Also at Sharif University of Technology, Tehran, Iran
40: Also at Department of Physics, University of Science and Technology of Mazandaran, Behshahr, Iran
41: Now at INFN Sezione di Bari a, Università di Bari b, Politecnico di Bari c, Bari, Italy
42: Also at Italian National Agency for New Technologies, Energy and Sustainable Economic Development, Bologna, Italy
43: Also at Centro Siciliano di Fisica Nucleare e di Struttura Della Materia, Catania, Italy
44: Also at Università di Napoli ‘Federico II’, Naples, Italy
45: Also at Riga Technical University, Riga, Latvia
Also at Consejo Nacional de Ciencia y Tecnología, Mexico City, Mexico

Also at IRFU, CEA, Université Paris-Saclay, Gif-sur-Yvette, France

Also at Institute for Nuclear Research, Moscow, Russia

Now at National Research Nuclear University ‘Moscow Engineering Physics Institute’ (MEPhI), Moscow, Russia

Also at St. Petersburg State Polytechnical University, St. Petersburg, Russia

Also at University of Florida, Gainesville, USA

Also at Imperial College, London, UK

Also at Moscow Institute of Physics and Technology, Moscow, Russia

Also at P.N. Lebedev Physical Institute, Moscow, Russia

Also at California Institute of Technology, Pasadena, USA

Also at Budker Institute of Nuclear Physics, Novosibirsk, Russia

Also at Faculty of Physics, University of Belgrade, Belgrade, Serbia

Also at Trincomalee Campus, Eastern University, Sri Lanka, Nilaveli, Sri Lanka

Also at INFN Sezione di Pavia a, Università di Pavia b, Pavia, Italy, Pavia, Italy

Also at National and Kapodistrian University of Athens, Athens, Greece

Also at Universität Zürich, Zurich, Switzerland

Also at Ecole Polytechnique Fédérale Lausanne, Lausanne, Switzerland

Also at Stefan Meyer Institute for Subatomic Physics, Vienna, Austria

Also at Laboratoire d’Annecy-le-Vieux de Physique des Particules, IN2P3-CNRS, Annecy-le-Vieux, France

Also at Şırnak University, Şırnak, Turkey

Also at Near East University, Research Center of Experimental Health Science, Nicosia, Turkey

Also at Konya Technical University, Konya, Turkey

Also at Faculty of Engineering, Istanbul University-Cerraphasa, Istanbul, Turkey

Also at Mersin University, Mersin, Turkey

Also at Piri Reis University, Istanbul, Turkey

Also at Adiyaman University, Adiyaman, Turkey

Also at Ozyegin University, Istanbul, Turkey

Also at Izmir Institute of Technology, Izmir, Turkey

Also at Necmettin Erbakan University, Konya, Turkey

Also at Bozok Universitesi Rektörlüğü, Yozgat, Turkey, Yozgat, Turkey

Also at Marmara University, Istanbul, Turkey

Also at Milli Savunma University, Istanbul, Turkey

Also at Kafkas University, Kars, Turkey

Also at Istanbul Bilgi University, Istanbul, Turkey

Also at Hacettepe University, Ankara, Turkey

Also at Vrije Universiteit Brussel, Brussel, Belgium

Also at School of Physics and Astronomy, University of Southampton, Southampton, UK

Also at IPPP Durham University, Durham, UK

Also at Monash University, Faculty of Science, Clayton, Australia

Also at Bethel University, St. Paul, Minneapolis, USA

Also at Karamanoğlu Mehmetbey University, Karaman, Turkey

Also at Bingol University, Bingol, Turkey

Also at Georgian Technical University, Tbilisi, Georgia

Also at Sinop University, Sinop, Turkey

Also at Mimar Sinan University, Istanbul, Turkey

Also at Istanbul Bilgi University, Istanbul, Turkey

Also at Erciyes University, Kayseri, Turkey

Also at Texas A&M University at Qatar, Doha, Qatar

Also at Kyungpook National University, Daegu, Korea