The Mechanical Effect of the Periodontal Ligament on Bone Strain Regimes in a Validated Finite Element Model of a Macaque Mandible

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The primary anatomical function of the periodontal ligament (PDL) is to attach teeth to their sockets. However, theoretical and constitutive mechanical models have proposed that during mastication the PDL redistributes local occlusal loads and reduces the jaw’s resistance to torsional deformations. These hypotheses imply that accurately modeling the PDL’s material properties and geometry in finite element analysis (FEA) is a prerequisite to obtaining precise strain and deformation data. Yet, many finite element studies of the human and non-human primate masticatory apparatus exclude the PDL or model it with simplicity, in part due to limitations in µCT/CT scan resolution and material property assignment. Previous studies testing the sensitivity of finite element models (FEMs) to the PDL have yielded contradictory results, however a major limitation of these studies is that FEMs were not validated against in vivo bone strain data. Hence, this study uses a validated and subject specific FEM to assess the effect of the PDL on strain and deformation regimes in the lower jaw of a rhesus macaque (Macaca mulatta) during simulated unilateral post-canine chewing. Our findings demonstrate that the presence of the PDL does influence local and global surface strain magnitudes (principal and shear) in the jaw. However, the PDL’s effect is limited (∼200–300 µε) in areas away from the alveoli. Our results also show that varying the PDL’s Young’s Modulus within the range of published values (0.07–1750 MPa) has very little effect on global surface strains. These findings suggest that the mechanical importance of the PDL in FEMs of the mandible during chewing is dependent on the scope of the hypotheses being tested. If researchers are comparing strain gradients across species/taxa, the PDL may be excluded with minimal effect on results, but, if researchers are concerned with absolute strain values, sensitivity analysis is required.

Keywords: finite element analysis, in vivo validation, biomechanics, mastication, rhesus monkey, sensitivity analysis
INTRODUCTION

The periodontal ligament (PDL) is a fibrous tissue of varying thickness (0.15–0.38 mm) that attaches the root cementum of each tooth to its surrounding alveolar bone (Berkovitz, 1990; Nanci and Bossardt, 2006). Previous studies have linked the PDL’s complex geometry (Berkovitz, 1990; Nanci and Bossardt, 2006; Ho et al., 2013) and material properties (heterogeneity, anisotropy, and viscoelasticity) (Andersen et al., 1991a; Van Driell et al., 2000; Dorow et al., 2003, 2014; Fill et al., 2011, 2012; Minch, 2013; Keilig et al., 2016) to its mechanical role in facilitating tooth mobility (Bien, 1966; Provatis, 2000; Pietrzak et al., 2002; Natali A. N. et al., 2004; Qian et al., 2009; McCormack et al., 2014) and absorbing and re-distributing occlusal loads (Reinhardt et al., 1984; Mohl, 1988; Daegling et al., 1992; Jeon et al., 1999; Rees, 2001; Poiate et al., 2009; Ren et al., 2010; Nikolaus et al., 2017). For instance, in a small-scale finite element analysis (FEA) of an isolated tooth-PDL-bone segment from an adult sow, Nikolaus et al. (2017) found that the PDL modeled with non-uniform thickness increased stresses in alveolar bone compared to models with uniform PDL thickness. From their results (Nikolaus et al., 2017) concluded that (a) the PDL protects the tooth roots by redirecting stresses into the alveolar bone and (b) PDL geometry (thickness) determines how these stresses are distributed across alveolar bone. Similarly, McCormack et al. (2017) showed that modeling the fibrous structures of the PDL (compared to modeling it as a solid object) in a section of a human mandibular corpus increased alveolar bone strains around the tooth socket (>100 με).

While these studies have used small-scale FEMs to highlight the importance of accurately modeling the PDL’s geometry, capturing the complex fibrous structure of the PDL in large-scale specimens (e.g., whole mandibles or crania) is not possible due to resolution constraints on computed tomography (CT) and μCT scans. Resolution and soft tissue contrast limitations also mean that PDL geometry is typically captured by selecting the space the PDL occupies and not the actual geometry of the tissue (Kucpzick et al., 2009; Cox et al., 2011; Panagiotopoulou and Cobb, 2011; Gröning and Fagan, 2012; Panagiotopoulou et al., 2017).

Further problems arise when assigning material properties to the PDL in FEA. Linear elastic models do not capture the true mechanical behavior of the PDL under load, which previous studies have shown to be non-linear (Bien, 1966; Wills et al., 1976; Fill et al., 2012). However, assigning complex (non-linear) material properties to the PDL in FEA is challenging. Viscoelastic models are able to combine time-dependent viscous (i.e., liquid phase) movement with instantaneous elastic, solid-like behavior (Fill et al., 2012) but data on the relationship between viscoelastic response and the structure of the PDL are limited (Natali A. et al., 2004; Qian et al., 2009; Zhang et al., 2014). In addition, time-dependent viscoelastic material properties cannot be assigned to static FEMs (Fill et al., 2012). While hyper-elastic models can be used in static FEMs (Fill et al., 2012), such models do not include the PDL’s fluid phase response to tension-compression loading (Fill et al., 2012). Also, hyper-elastic models are described by a stored energy function that is load case and material specific. As such, the material parameters used in hyperelastic models are ideally derived from load case and tissue-specific experimental data. Finally, while multi-phase models allow for the coupling of viscoelastic and hyper-elastic constitutive models to more accurately represent the global behavior of the PDL the lack of sufficient data on the viscoelastic properties of the PDL limits our ability to design these multi-phase models (Fill et al., 2012).

Due to these modeling limitations, in large-scale and static FEMs (e.g., mandible/crania) the PDL is frequently modeled as a linear elastic, homogeneous, isotropic tissue, and assigned a single Young’s Modulus (E) value (e.g., Slater et al., 2009, 2010; Cox et al., 2011; Panagiotopoulou and Cobb, 2011; Porro et al., 2013; Panagiotopoulou et al., 2017). However, the PDL has both a time- and direction-sensitive response to load (Sakada and Kamio, 1971; Trulsson et al., 1992), and as a result variation in strain results remains unclear.

Other studies exclude the PDL entirely from large-scale FEMs of the cranium or mandible (Dumont et al., 2005, 2009; Strait et al., 2005, 2007, 2009; Wroe et al., 2007; Slater et al., 2010; Bright and Rayfield, 2011; Bright, 2012; Figueirido et al., 2014; Fitton et al., 2015; Smith et al., 2015a,b; Toro-Ibacache and O’Higgins, 2016; Toro-Ibacache et al., 2016). However, sensitivity analysis of the effects of excluding the PDL in whole FEMs has yielded conflicting mechanical results (Gröning et al., 2011, 2012; Wood et al., 2011; Gröning and Fagan, 2012; Grosse et al., 2012). An early study by Daegling et al. (1992) investigating the influence of the PDL on the mechanics of the mandible proposed that inclusion of the PDL in FEMs, even when modeled with simplicity may affect the transmission of torsional shear stresses from the bone-tooth interface into the alveoli. Researchers also proposed that the presence of the PDL would reduce the torsional rigidity of the jaw (defined as a structure’s ability to resist deformations brought about by twisting moments; Daegling et al., 1992). As a decrease in torsional rigidity would constitute decreased resistance to both axial and shear strains (Biewener et al., 1992), it follows that including the PDL in large scale FEMs of the crania or mandible would result in an increase in principal and shear strains across the jaw. A later study of the Macaca fascicularis mandible found that FEMs that model bone and teeth as continuous structures (i.e., exclude PDL) report strains lower than those found in vitro, lending partial support to the hypothesis that the PDL decreases overall rigidity of the jaw (Marinescu et al., 2005). However, their study lacked a FEM that included the PDL for comparison.

More recently, Gröning et al. (2011) FEA of a human mandible showed that inclusion of the PDL increased principal strains in the whole mandible, with ≥500 με increase in areas in the mandibular corpus. The authors also recorded an increase in principal strains inferior to the constrained tooth and proposed that inclusion of the PDL in FEA reduces the stiffness of the
human mandible (Gröning et al., 2011). In a follow-up sensitivity analysis, Gröning et al. (2012) found that inclusion of the PDL in a different FEM of the human mandible increased strain magnitudes in the mandibular corpus by more than 40%. By contrast, Wood et al. (2011) tested the effect of the PDL on deformations of a Cebus (now Sapajus apella) cranium using FEA and found that when modeled as an isotropic, homogeneous and linear elastic tissue, inclusion of the PDL had a localized effect on von Mises stress in alveolar bone but only subtle effects on von Mises stress elsewhere in the cranium, even after varying the PDL material properties (linear elastic, hyper elastic, and viscoelastic).

The divergent findings of Gröning et al. (2011) and Wood et al. (2011) have been attributed to a variety of factors, including differences in species (brown capuchin monkey vs. modern human), skeletal structure being modeled (cranium vs. mandible), the size of the tooth root relative to the skeletal structure (teeth to maxilla vs. teeth to mandible), and boundary conditions in the FEA (direct constraint of condyles vs. constraining temporomandibular joint modeled as a layer of soft tissue; Gröning and Fagan, 2012; Grosse et al., 2012). Importantly, however, to our knowledge, no study has assessed the sensitivity of various modeling conditions of the PDL using a subject-specific FEM, validated against in vivo bone strain data. Considering the assumptions made when modeling the PDL as a geometrically simplified, homogeneous and isotropic tissue in static, large scale FEMs, it is important to test whether such modeling assumptions affect bone strain results from FEA and whether they yield bone strain results close to in vivo bone strain data.

To this end, our study investigated the mechanical influence of the PDL on strain regimes in a validated static FEM of a female rhesus monkey (Macaca mulatta) during simulated unilateral post-canine chewing. We tested two hypotheses:

**Hypothesis 1:** Inclusion of the PDL (and associated alveolar tissues), creating a more compliant interface between tooth and bone, decreases torsional rigidity of the jaw and increases global surface strain magnitudes (surface strains across the entire jaw). Exclusion of the PDL (and associated alveolar tissues) increases the jaw’s torsional rigidity and decreases global surface strains (Daegling et al., 1992; Gröning et al., 2011). Based on this hypothesis we made the following three predictions:

1. When the PDL is included in FEMs of the jaw, progressive increases in its Young’s Modulus (i.e., decreases in its compliance) will increase the torsional rigidity of the jaw, resulting in progressively lower global surface principal strain (ε₁ — maximum principal strain and ε₂ — minimum principal strain) magnitudes.
2. The FEM of the jaw that excludes the PDL will experience lower global surface principal strain magnitudes during simulated chewing compared with the FEM that includes the PDL (Gröning et al., 2011).
3. The FEM of the jaw that includes the PDL will experience greater torsion of the balancing- and working-side corpora, and higher associated shear strains, than the FEM that excludes the PDL.

**Hypothesis 2:** The PDL acts to redirect masticatory stresses from the tooth roots to the alveolar bone. We predict that FEMs that exclude the PDL will have higher strains in the tooth roots compared with FEMs that include the PDL (McCormack et al., 2017; Nikolaus et al., 2017).

**METHODS**

To test our hypotheses we used a previously published FEM of a rhesus macaque mandible (Panagiotopoulou et al., 2017) and validated our FEMs against in vivo bone strain data. The details of capturing model geometry, segmentation, and material property assignment for the cortical bone, trabecular tissue, teeth and PDL are described in full elsewhere (Panagiotopoulou et al., 2017). As the PDL itself cannot be visualized in CT, its geometry was demarcated as a continuous, non-uniform space between the tooth root and alveolar bone (spanning 3–6 voxels), and was segmented using a combination of manual and automatic methods (Panagiotopoulou et al., 2017). The FEM was assigned 80 heterogeneous and orthotropic material properties to the cortical bone using data derived from an ex vivo experiment using the ultrasound wave technique (Dechow et al., 2017) and a linear theoretical model to relate Young’s modulus and Poisson’s ratio to the density of the calibrated CT scans (Dechow et al., 2017; Panagiotopoulou et al., 2017). We assigned the data from the theoretical model to our FEMs by using the formula below to define the relationship between grayscale values (GV) of the CT scans, apparent density and parameters of the material properties (E, v):

\[
\text{Poisson's ratio (v)} = 0.400595880819907 + \\
- 0.00000913165104192569 \times \rho
\]

\[
\text{Young's Modulus (E)} = -2.7501977952777819 + \\
0.0082389155811676013 \times \rho
\]

where Density (ρ) = −0.01979662 × 1.0577433 × GV.

Full details of the experimental protocol for material testing and the development of the theoretical model are provided in Dechow et al. (2017) and Panagiotopoulou et al. (2017), respectively. Isotropic and homogeneous elastic material properties were assigned to the bone screws (E = 105 000 MPa; v = 0.36), teeth (E = 24 500 MPa; v = 0.49), PDL (E = 0.68 MPa; v = 0.49), and trabecular bone (E = 10 000 MPa; v = 0.3) (Panagiotopoulou et al., 2017). Bone screws were implanted in the mandible to measure three dimensional (3D) rigid body kinematics of the mandible during the post-canine unilateral chewing modeled in this study (Iriarte-Diaz et al., 2011; Ross et al., 2012; Panagiotopoulou et al., 2017).

**PDL Variants**

To determine whether the PDL influenced the mechanics of the jaw during post-canine chewing, we compared the original validated FEM (=PDL model) against models that:
a. entirely excluded the PDL by assigning it material properties of the surrounding teeth (\(E = 24\,500\) MPa and \(v = 0.49\)) (NO PDL Model) (Supplementary Figure S1).

b. varied the Young's Moduli between 0.07, 0.18, 13.8, and 1,750 MPa (Models 1–4, respectively) corresponding to the published \(E\) data experimentally determined from humans and dogs (Thresher and Saito, 1973; Yettram et al., 1977; Takahashi et al., 1980; Andersen et al., 1991a,b; Goel et al., 1992; Cattaneo et al., 2005; Li et al., 2006). The Poisson’s ratio of the PDL was kept constant at \(v = 0.49\), as previous sensitivity studies showed that varying the Poisson’s ratio between 0.45–0.49 had no effect on FEM behavior (Gröning et al., 2011; Wood et al., 2011).

### Loading Models

All FEMs were loaded using subject-specific muscle force vectors that simulated unilateral post-canine chewing. Muscle-force data were derived from an in vivo experiment during which the animal was chewing on nuts (almond, cashew, brazil nut, pecan, walnut, seeds). Detailed experimental protocols for the in vivo electromyography (EMG) recording and post-processing is similar to the one provided in Panagiotopoulou et al. (2017), when the animal was chewing on soft food. Briefly, all muscle-force vectors were derived from a combination of in vivo raw EMG signals collected when the animal was chewing on nuts and ex vivo muscle physiological cross-sectional area (PCSA) analysis to estimate the maximum force potential of each muscle (Panagiotopoulou et al., 2017). To assign the muscle-force vectors to our FEMs we selected surface nodes representing the insertion areas of the working- and balancing-side jaw-elevator muscles (deep and superficial masseter, anterior and posterior temporalis, medial pterygoid) determined from dissection pictures of the experimental subject. Force magnitude of each muscle was calculated by multiplying the estimated PCSA by 30 N/cm², an estimate of the muscle-specific tension (Sinclair and Alexander, 1987), scaled to the mean normalized EMG amplitude at the time of maximum bone strain. The directional components of the force vectors were calculated using the cranial and mandibular attachments of each muscle, determined from dissection images of the experimental subject. All muscle force data are listed in Supplementary Table S1.

To simulate bite force, we constrained the occlusal surfaces of the working (left) premolars and first molar and fixed them against translations in all directions (Panagiotopoulou et al., 2017). To allow for lateral transverse bending of the mandible we selected one node at the top of each mandibular condyle and fixed the right (balancing-side) condyle against translations in the anterior-posterior and superior-inferior directions but allowed medio-lateral translation. The working-side mandibular condyle was fixed against translation in all directions and rotation was permitted at both condyles (Panagiotopoulou et al., 2017). To prevent friction between internal/embedded structures within FEMs (e.g., PDL and internal surfaces of cortical bone), all adjacent surfaces were bound together with tie constraints. All FEMs were solved using the Abaqus CAE Simulia software v2016 default implicit direct static solver (Dassault Systèmes, Velizy-Villacoublay, France). Average solution time (4 processors and 8 tokens) was \(\sim 10\) min per model.

### Model Validation

To validate our PDL and NO PDL models we compared strains from our FEMs to in vivo mandibular bone strains collected from the same individual while the animal was chewing on nuts. Experimental protocols for the collection and analysis of the in vivo strain gauge data are detailed elsewhere (Panagiotopoulou et al., 2017). Briefly, in vivo strain data were collected from three rosette strain gauges surgically bonded to the left (working side) mandible. Two were fixed to the buccal aspect of the working-side corpus (below the first molar, beside the most anterior attachment of the superficial masseter muscle), one close to the inferior border (LLAT) and the other close to the horizontal midline (ULAT). The third gauge (MED) was fixed to the lingual surface of the working-side corpus, inferior to the insertion of the mylohyoid muscle, beneath the left first molar. To locate the gauge sites in the FEM, Panagiotopoulou et al. (2017) overlayed FE mesh files with radiographs taken of the macaque head shortly after surgical implantation of the gauges, aligning them manually to achieve best fit. Strain tensors from the surface elements at these locations then were obtained and rotated to match the coordinate system of the corresponding strain gauge. These strain tensors were used to calculate the magnitude and direction of principal strains at the gauge locations in the FEMs, allowing for comparison to in vivo strain data. Raw in vivo strains from the strain gauge locations when the animal was chewing on nuts are provided in Supplementary Table S2.

### Testing Predictions

Hypothesis 1: Inclusion of the PDL (and associated alveolar tissues), creating a more compliant interface between tooth and bone, decreases the torsional rigidity of the jaw and increases global surface strains; absence of the PDL (and associated alveolar tissues) increases the jaw’s torsional rigidity and decreases global surface strains.

Prediction 1: When the PDL is included in FEMs of the jaw, progressive increases in its Young's Modulus (i.e., decreases in its compliance) will increase the torsional rigidity of the jaw, resulting in progressively lower global surface principal strain (\(\varepsilon_1\)—maximum principal strain and \(\varepsilon_2\)—minimum principal strain) magnitudes.

To determine if increasing the PDL's Young's Modulus increases the jaw's torsional rigidity and progressively decreases principal strain magnitudes we plotted the maximum and minimum principal strains from homologous locations across the working-side (left) corpus in Models 1–4. We also calculated element level differences in principal strain magnitudes in the cortical bone of Models 1 and 4 and have outlined specific anatomic locations for comparison (Supplementary Figure S2). To calculate element level differences, we exported principal strains from Abaqus CAE Simulia (v2016), and used custom written MatLab code to calculate the element level difference in results and projected these values onto the 3D model of cortical bone.
Prediction 2: The FEM of the jaw that excludes the PDL will experience lower global surface principal strain magnitudes during simulated unilateral post-canine chewing than the FEM including the PDL.

To quantify differences in principal strains we calculated elemental differences in principal strains found in the cortical bone and trabecular bone tissue of the PDL and NO PDL models, using the same method outlined for Prediction 1.

Prediction 3: The FEM of the jaw that includes the PDL will experience greater torsion of the balancing- and working-side corpora, and higher associated shear strains, than the FEM that excludes the PDL.

To quantify whether excluding the PDL lowers shear strains associated with torsion of the working- and balancing-side corpus we calculated elemental differences in the sagittal-XY, frontal-XZ and transverse-YZ shear strains in the cortical bone.

Hypothesis 2: The PDL acts to redirect masticatory stresses from the tooth roots to the alveolar bone.

Prediction: We predict that FEMs without the PDL will have higher strains in the tooth roots than FEMs with the PDL.

To evaluate whether the PDL redirects masticatory stresses from the tooth roots to the alveolar bone we compared strains in the alveolar tissues (teeth and PDL) of the PDL and NO PDL models. We calculated elemental differences in principal ($\varepsilon_1$ and $\varepsilon_2$) and shear (sagittal-XY, frontal-XZ and transverse-YZ) strains found in the 3D geometries of the PDL and teeth.

RESULTS

Model Validation

In two of the three gauge sites (ULAT and LLAT), median principal strain magnitudes from both the PDL and NO PDL FEMs are within 1.5*interquartile range (IQR) of the in vivo data (Figure 1). At the third gauge site, only the $\varepsilon_2$ principal strains from the PDL model where within 1.5*IQR of the in vivo data (Table 1), though principal strains from both FEMs were within the broader range of those recorded in vivo. At all three gauge locations principal strain orientations from FEMs were within the range of those measured in vivo (Figure 2).

Hypothesis 1: Inclusion of the PDL (and associated alveolar tissues), creating a more compliant interface between tooth and bone, decreases the torsional rigidity of the jaw and increases global surface strains; absence of the PDL (and associated alveolar tissues) increases the jaw’s torsional rigidity and decreases global surface strains.

Principal strain comparisons in models that vary the Young’s Modulus of the PDL (0.07–1.750 MPa) support Prediction 1 such that increasing the Young’s Modulus of the PDL decreases global principal strains (Supplementary Figure S3). Plotting the elemental differences of $\varepsilon_1$ strain magnitudes between the FEMs with the extreme Young’s moduli [Model 1 ($E = 0.07$ MPa) vs. Model 4 ($E = 1,750$ MPa)] showed that Model 4 had $\varepsilon_1$ strains higher than Model 1 (>100 $\mu$ε) along the buccal aspect of the working-side corpus at the level of the premolars (Figure 3). Model 4 yielded lower (>100 $\mu$ε) $\varepsilon_1$ strains than Model 1 at the alveoli of the post canine teeth of both the working- and balancing- sides and the lingual symphysis. In addition, Model 4 experienced marginally lower (~50 $\mu$ε) and considerably lower (>100 $\mu$ε) $\varepsilon_2$ strains than Model 1 in the alveoli and in the labial symphysis (Figure 3).

Plots of element-level differences between PDL and NO PDL cortical bone strains showed that Prediction 2 was partially supported. Exclusion of the PDL resulted in lower principal ($\varepsilon_1$ and $\varepsilon_2$) strains on both the working- and balancing-side mandible (Table 2; Figure 4). However, at various mandibular sites the NO PDL model yielded $\varepsilon_1$ magnitudes higher (diff. of 50–100 $\mu$ε) than the PDL model (Table 2; Figure 4). Principal strain comparisons at the trabecular tissue level between the PDL and NO PDL FEMs showed similar patterns to cortical bone. The NO PDL model had trabecular bone $\varepsilon_1$ and $\varepsilon_2$ magnitudes lower than the PDL model in various locations across the mandible (Supplementary Table S3: Supplementary Figure S4) and $\varepsilon_3$ magnitudes higher than the PDL in the trabecular bone of the alveoli (Supplementary Table S3; Supplementary Figure S4).

Shear strain comparisons between the PDL and NO PDL models supported Prediction 3 that exclusion of the PDL in FEA reduces torsion in the balancing-and working-side corpora (Figure 5).

We observed lower frontal ($\varepsilon_{13}$) shear strains in the NO PDL model in the anterior corpus (decrease of ~100 $\mu$ε) (Figure 5) and in the alveolar bone of the balancing-side $M_3$ and working-side P$\overline{3}P_1M_1$ (decrease of more than 500 $\mu$ε). We found higher frontal shear strains (~100 $\mu$ε) in the NO PDL model at the working-side alveoli of P$\overline{3}P_1M_1$ lingually.

We measured lower (>500$\mu$ε) transverse ($\varepsilon_{23}$) shear strains in the NO PDL than the PDL model (Figure 3), except for slightly higher (~100 $\mu$ε) transverse shear strains in the NO PDL model at the anterior corpus of the balancing side (Figure 5).

Sagittal shear strains ($\varepsilon_{12}$) were lower (~100 $\mu$ε) in the NO PDL model in the alveolar bone and the lingual symphysis (Figure 5). Particularly large decreases in $\varepsilon_{12}$ (<500 $\mu$ε) were found in the alveolar bone below the working side molars and balancing side $M_3$ (Figure 5). However, sagittal shear strains were higher in the NO PDL model in the working-side lingual anterior corpus (Figure 5).

All raw data used in Table 2 and to generate Figures 3–5; Supplementary Figures S3, S4 are available at figshare (Mehari Abraha et al., 2019).

Hypothesis 2: The PDL acts to redirect masticatory stresses from the tooth roots to the alveolar bone.

The differences between principal strains of PDL and NO PDL models in the alveolar tissues (teeth and PDL) were the largest recorded in the entire FEM (diff. >1,000 $\mu$ε) (Figures 6, 7 vs. Figure 4), demonstrating that at a local level, excluding the PDL increased strains in the tooth roots and decreased strains in the PDL. Thus, our prediction that FEMs without the PDL will have higher strains in the tooth roots than FEMs with the PDL is supported.

Detailed analysis of principal strains in the dentition showed that in the tooth roots of balancing- and working-side post canine teeth the NO PDL model had higher (increase of ~250 $\mu$ε) $\varepsilon_1$ and $\varepsilon_2$ strains than the PDL model (Figure 6). The greatest increase in $\varepsilon_2$ strains was found in the first molar.
on the working side (difference $>\sim 500 \, \mu e$) (Figure 6). There were some locations (e.g., tooth-bone junction point) in the balancing- and working-side molars where the NO PDL model had lower $\varepsilon_1$ and $\varepsilon_2$ strains (decrease of $>\sim 500 \, \mu e$) (Figure 6). The NO PDL model also experienced higher sagittal (XY) shear strain in the roots of the working side $P_3 P_4 M_1$, higher frontal (XZ) shear strain in the roots of the working side molars (increase of $>\sim 250 \, \mu e$) and higher transverse (YZ) shear strain (increase of $>\sim 250 \, \mu e$) in the roots of the balancing side molars (Figure 6).

In the periodontal ligament itself, the NO PDL model experienced lower $\varepsilon_1$ and $\varepsilon_2$ strains (decrease of $>500 \, \mu e$) than the PDL model (Figure 7). Specifically, the ligament tissue surrounding the working-side premolars and first molar, and the balancing-side third molar had $\varepsilon_1$ strains that were higher than the NO PDL model by more than 500 $\mu e$ (Figure 7). Similarly, $\varepsilon_2$ strains were more than $\sim 500 \, \mu e$ higher in the PDL model in the ligament tissue of the working-side premolars and first molar and the balancing-side third molar (Figure 7). The NO PDL model also had sagittal (XY), frontal (XZ) and transverse (YZ) shear strains more than 1,000 $\mu e$ lower in the periodontal ligament surrounding the working-side post-canine dentition and the balancing-side molars (Figure 7).

All raw data used to generate Figures 6, 7 are available at figshare (Mehari Abraha et al., 2019)
**FIGURE 2** | (A) Mandible model with markers indicating locations of the ULA T (red), LLAT (green), and MED (blue) strain gauge sites. (B) CT scan slices of mandible indicating the breakdown of the PDL and NO PDL models. (C) Polar histogram of the distribution of ε₁ orientations (in degrees) at the LLAT, ULAT, and MED gauge sites of PDL and NO PDL FEMs compared to the in vivo experiment. Red solid lines indicate the mean orientation. Black bars and blue circles represent the range of FEMs and in vivo data, respectively.

**FIGURE 3** | Color plots of differences in maximum (ε₁) and minimum (ε₂) principal strain magnitudes between Model 1 (PDL E = 0.07 MPa) and Model 4 (PDL E = 1,750 MPa). Pairs of FEMs are compared by mapping the cortical bone surface distribution of element level differences in principal strains between the two models onto the surfaces of the model. Panels compare ε₁ and ε₂ magnitudes between the model pairs in four views. Scale bars to the right of each panel indicate the difference in principal strains (µε) between models. Areas of greater difference in results from Models 1 and 4 are indicated by darker colors, while lighter colors indicate areas of high similarity.
TABLE 2 | Summary of differences in cortical bone of NO PDL and PDL models.

| Location | Direction of difference | Magnitude of difference |
|----------|-------------------------|-------------------------|
| **ε₁—MAXIMUM PRINCIPAL STRAIN** |
| Working (left) side | | |
| Buccal alveoli, inferior to P₂P₃M₂M₃ | NO PDL < PDL | >200 µε |
| Lingual alveoli, inferior to P₂P₃M₁M₂ | NO PDL < PDL | >200 µε |
| Temporomandibular joint constraint point of condylar process | NO PDL < PDL | >200 µε |
| Posterior aspect of buccal corpus | NO PDL < PDL | ~50 µε |
| Anterior aspect of buccal corpus | NO PDL > PDL | ~50 µε |
| Posterior aspect of lingual corpus | NO PDL > PDL | ~50 µε |
| Balancing (right) side | | |
| Temporomandibular joint constraint point of condylar process | NO PDL < PDL | >200 µε |
| Lingual and buccal alveoli inferior to M₁M₂ | NO PDL < PDL | >200 µε |
| Superior aspect of lingual corpus | NO PDL < PDL | ~50 µε |
| Retromolar region | NO PDL > PDL | ~50 µε |
| Symphysis | | |
| Superior and inferior tori of lingual symphysis | NO PDL < PDL | ~50 µε |
| Inferior aspect of labial symphysis | NO PDL < PDL | ~50 µε |
| **ε₂—MINIMUM PRINCIPAL STRAIN** |
| Working side (left) side | | |
| Buccal alveoli, inferior to P₂P₃M₁M₂M₃ | NO PDL < PDL | >200 µε |
| Lingual alveoli, inferior to P₂P₃M₁M₂ | NO PDL < PDL | >200 µε |
| Superior aspect of lingual anterior corpus | NO PDL < PDL | ~50 µε |
| Inferior aspect of lingual ramus | NO PDL > PDL | ~50 µε |
| Balancing side | | |
| Buccal and lingual corpus inferior to balancing side M₃ | NO PDL < PDL | >200 µε |
| Inferior aspect of inferior | NO PDL < PDL | >200 µε |
| Posterior aspect of ramus superiorly | NO PDL < PDL | ~50 µε |
| Lingual corpus | NO PDL < PDL | ~50 µε |
| Buccal posterior aspect of corpus | NO PDL > PDL | ~ 50 µε |
| Symphysis | | |
| Lingual inferior and superior aspect | NO PDL < PDL | ~50 µε |
| Labial inferior and superior aspect | NO PDL < PDL | ~50 µε |

FIGURE 4 | Color plots of differences in maximum (ε₁) and minimum (ε₂) principal strain magnitudes between models that include (PDL Model) and exclude (NO PDL Model) the periodontal ligament. Pairs of FEMs are compared by mapping the cortical bone surface distribution of element level differences in principal strains between the two models onto the surfaces of the model. Panels compare ε₁ and ε₂ magnitudes between the model pairs in four views. Scale bars to the right of each panel indicate the element level difference in principal strains (µε) between models. Areas of greater difference in results from PDL and NO PDL models are indicated by darker colors, while lighter colors indicate areas of high similarity.
DISCUSSION
Comparison of Results With Previous Studies of the PDL
While our findings partially confirm the hypothesis that the presence of the PDL decreases the torsional rigidity of the jaw and affects global surface strains, the degree to which our results are consistent with existing literature varies. Gröning et al. (2011) compared a PDL FEM ($E = 0.01$ MPa) to a NO PDL FEM where the PDL was modeled as cortical bone ($E = 17$ 000 MPa) and found that excluding the PDL decreased global surface principal strains. However, we did not find the same degree of variation between our PDL and NO PDL FEMs. When Gröning et al. (2011) contrasted PDL and NO PDL FEMs, they found $\varepsilon_1$ differences $\geq 500$ $\mu$ε in several areas in the cortical bone, namely in the labial symphysis ($\varepsilon_1$ was 543 $\mu$ε higher in PDL model) and below the post-canine dentition on the balancing side ($\varepsilon_1$ was 519 $\mu$ε higher and $\varepsilon_2$ was 546 $\mu$ε lower in the PDL model). In contrast, the greatest degree of variation noted in our study was in the periodontal tissue (diff. $>1,000$ $\mu$ε–Figure 7), and only smaller differences were found elsewhere in the mandible (Table 2; Figure 4).

Differences between our results and those of Gröning et al. may be attributed to differences in the boundary conditions of the FEMs (Gröning and Fagan, 2012; Grosse et al., 2012). While we allowed medio-lateral translation of one condyle to allow for lateral transverse bending of the jaw (Hylander, 1984, 1985; Panagiotopoulou et al., 2017), Gröning et al. (2011) fixed both condyles against translation in all directions using a compliant pad of soft tissue. In their study (Gröning et al., 2011) conducted sensitivity analysis to determine whether constraining the jaw through a compliant pad of soft tissue influenced results, and found that constraining the condyles directly did not affect their findings (i.e., the presence of the PDL still had a large effect on local and global principal strains). However, to the best of our knowledge, they did not run a model where mediolateral translation of one condyle was allowed. To test whether these condylar constraints affected model sensitivity to the PDL, we over-constrained our PDL and NO PDL models (i.e., condyles constrained in all directions) and compared bone strain regimes. We found no increased sensitivity to the presence of the PDL (i.e., no pronounced change to our results) (Supplementary Figure S5).

Disparity between our results and those of Gröning et al. (2011) could also be due to variation in the directional forces and the co-activation of the adductor jaw muscles. While our model applied muscle forces associated with unilateral post-canine chewing (based on in vivo and subject-specific experiments), Gröning et al. (2011) applied muscle force vectors associated with unilateral molar clenching (derived from Nelson, 1986; Korioth et al., 1992; Korioth and Hannam, 1994; van Eijden et al., 1995, 1996). To test whether different feeding behaviors (post-canine chewing vs. clenching) could influence the difference in strain regimes between the PDL and NO PDL models we re-ran our models using the muscle activation scaling of the major jaw-closing muscles provided in Gröning et al. (2011), originally reported in Nelson (1986). Though we were unable to include the directional component of the

FIGURE 5 | Color plots of differences in shear strain magnitudes between models that include (PDL Model) and exclude (NO PDL Model) the periodontal ligament. Pairs of FEMs are compared by mapping the cortical bone surface distribution of element level differences in shear strains between the two models onto the surfaces of the model. Panels compare $\varepsilon_{12}$ (sagittal), $\varepsilon_{13}$ (frontal), and $\varepsilon_{23}$ (transverse) shear strain magnitudes between the model pairs in four views. Scale bars to the right of each panel indicate the difference in strains ($\mu$ε) between models. Areas of greater difference in results from PDL and NO PDL models are indicated by darker colors, while lighter colors indicate areas of high similarity.
FIGURE 6 | Color plots of differences in strain magnitudes found in the teeth of FEMs that include (PDL Model) and exclude the periodontal ligament (NO PDL Model).

Pairs of FEMs are compared by mapping the cortical bone surface distribution of element level differences in principal strains between the two models onto the surfaces of the teeth. (A) Shows differences in $\varepsilon_1$ and $\varepsilon_2$ principal strains magnitudes. (B) Shows differences in sagittal ($\varepsilon_{12}$), frontal ($\varepsilon_{13}$), and transverse ($\varepsilon_{23}$) shear strain magnitudes between model pairs in four views. Scale bars to the right of each panel indicate the element level difference in strains ($\mu\varepsilon$) between models. Areas of greater difference in results from PDL and NO PDL models are indicated by darker colors, while lighter colors indicate areas of high similarity.

muscle force vectors used by Gröning et al. (2011) and we did not include the inferior head of the lateral pterygoid muscle, we found that assigning muscle forces associated with clenching did result in a greater sensitivity of our FEM to the presence/absence of a PDL (Supplementary Figure S6). Considering these additional findings, we propose that variations in the activation peaks of the major muscles of mastication in clenching vs. chewing behaviors, particularly the working- and balancing-side superficial masseters and medial pterygoids, may have altered the twisting moments of the corpora and in turn, affected the FEMs sensitivity to the presence of the PDL. This coupled with variations in mandibular morphology and masticatory musculature between humans and macaques, may account for the discrepancies between our results and those of Gröning et al. (2011).

Wood et al. (2011), in contrast to Gröning et al. (2011), found that excluding the PDL resulted in lower principal strains in the canine and molar alveolar regions of the cranium. However, Wood et al. (2011) found “negligible” differences elsewhere in the mandible, while we found differences of $\sim 200 \mu\varepsilon$. Divergence between our results and those of Wood et al. (2011) could be attributed to differences in the size of the dentition relative to the skeletal element (cranium vs. mandible), as larger tooth roots would increase the jaws resistance to torsional deformation and decrease a jaw FEMs sensitivity to the PDL. However, such incongruity could also be attributed to differences in the methods of comparison between FEM strain regimes. The differences between PDL and NO PDL models in our study are difficult to distinguish when contrasting color plots of maximum and minimum principal strains across the mandible (Supplementary Figures S7, S8) but are much easier to identify in element differential plots between models (Figure 4). Hence, while Wood et al. (2011) report negligible differences between models that include and exclude the PDL in areas away from the
alveoli, it is possible that with element level comparisons these differences may become more apparent.

We observed that excluding the PDL from the FEMs decreased strains in the alveolar bone but increased strains in the tooth roots (Figures 6, 7). These results broadly support the hypotheses that the PDL transmits/redistributes strains across the bone-PDL-tooth interface (McCormack et al., 2017; Nikolaus et al., 2017) while also providing further credibility to the specific hypothesis proposed by Nikolaus et al. (2017) that under masticatory loads the PDL acts to shield the tooth roots by redirecting strains to the alveolar bone. Their hypothesis was previously supported by high resolution, small scale testing of strains in sections of the human and pig mandibular corpora (McCormack et al., 2017; Nikolaus et al., 2017). However, our findings highlight that even in large scale FEA (where the PDL is modeled as a simplified, linear elastic tissue) the PDL’s mechanical effect on the local strain environment is still evident.

Implications for Modeling the PDL in FEA

Overall, our results demonstrate that the PDL has some effect on the global surface maximum and minimum principal strains in the macaque mandible during unilateral post-canine chewing. Yet it is worth noting that comparisons of corpus surface strains between the FEMs (with and without the PDL) to in vivo strain gauge data showed that both FEMs yield strain magnitudes and orientations within the range of in vivo bone strains (Figures 1, 2) (Panagiotopoulou et al., 2017). Thus, whilst the PDL tissue has some localized effect on strain magnitudes across the jaw when included in FEA, it does not appear to substantially alter the mechanical behavior of the jaw during unilateral post-canine chewing. Therefore, if the hypotheses being tested relate to large scale differences in the magnitude/orientation/patterns of principal strains across individuals or species under these loading conditions, it is unlikely that excluding the PDL or varying its Young’s Modulus within the published range of 0.07–1,750 MPa will have a large effect on research findings. If, however, the hypotheses are concerned with small-scale differences in principal strains between models (e.g., element-to-element comparison) then variation in the Young’s Modulus of the PDL and/or exclusion of the PDL tissue may result in strain differences, and sensitivity analysis is required.
A limitation of our study is that we tested the effect of the PDL under very specific masticatory loading conditions (post-canine chewing on nuts). As outlined by Hylander (1979) the position of the bite point may affect torsion of the corpora. For example, bite forces that pass lateral to the longitudinal axis of the corpora may result in twisting the corpus such that the inferior border inverts and the alveolar process everts, while forces that pass medial to the longitudinal axis may do the opposite (Hylander, 1979).

Further, our study was limited to a single species (M. mulatta) and as discussed previously (Daegling and Hylander, 1998; Daegling, 2007), different corporal geometries across species may affect the torsional rigidity of the jaw. Given that any effect on mandibular torsion may affect a FEMs sensitivity to the PDL, further sensitivity studies (using a combination of in vivo data collection and computer modeling) testing other loading conditions (e.g., incisor biting, unilateral biting) and/or other primate species are needed (Picton and Wills, 1978; Mow et al., 1984; Dorow et al., 2003; Natali A. et al., 2004; Wang et al., 2012; Sandino et al., 2015).

Our study did not account for the effect of variation in the PDL’s thickness on local/global surface strain regimes. A previous small-scale FEA study captured the geometry of a molar tooth-PDL-bone complex from a pig mandible using μCT scans (pixel resolution 0.012 mm) and found that the PDL’s thickness varied between 0.05 and 0.5 mm from region to region within the tooth root (median 0.21 mm; Nikolaus et al., 2017). However, in the case of mesh-based FEA, automatic non-manifold mesh generation requires a minimum thickness of 3 voxels for each structure, as fewer voxels causes unresolvable overlapping and intersecting triangles. Thus, accurately capturing variation in PDL thickness (~0.05–0.5 mm) would require a scan resolution where pixel size is ~0.016 mm, which was outside the range of our scans (0.2 mm).

Lastly, our study focused on the effect of the PDL when modeled with simplicity in a static linear simulation of the entire mandible. Modeling the PDL as a time-dependent tissue would likely provide us with greater insight on the mechanical function of the PDL during chewing; however, it would require the creation of a dynamic FEM, which was outside the scope of this study. Modeling the PDL as a hyperelastic tissue (e.g., Wood et al., 2011; Nikolaus et al., 2017) in a static simulation requires the definition of load- and tissue-specific material parameters, and validation and calibration of these parameters using load- and tissue-specific experimental data. While we did not include a FEM in which the PDL is modeled as a hyperelastic or viscoelastic tissue, we can note that Wood et al. (2011) compared a static FEM where the PDL was included and modeled as linear elastic ($E = 0.68$ MPa, $v = 0.49$) to a static FEM where the PDL was modeled as a Mooney Rivlin hyper-elastic material, with parameters derived from Genna et al. (2007). They also compared a dynamic model where the PDL was assigned linear elastic properties to a dynamic model where the PDL was modeled as viscoelastic (using the Maxwell chain model outlined in Natali A. et al. (2004)). They found that that inclusion of hyperelastic or viscoelastic material properties for the PDL in the respective static and dynamic simulations had no visible effect on global surface strain regimes in areas away from the loaded teeth.

DATA AVAILABILITY STATEMENT

The datasets (results from finite element models) for this study can be found at Monash figshare (Mehari Abraha et al., 2019).

ETHICS STATEMENT

Ethical review and approval was not required as this was a computer-based study. All in vivo data used in this study were collected as part of a previous publication (Panagiotopoulou et al., 2017).

AUTHOR CONTRIBUTIONS

HM, OP, CR, and AT designed the study. OP built and solved the PDL FEM. HM built and solved the NO PDL FEM. HM, JI-D, and OP contributed into the numerical analysis of the FEMs. HM wrote the manuscript with critical analysis and editing by OP, JI-D, AT, and CR.

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SUPPLEMENTARY MATERIAL

The Supplementary Material for this article can be found online at: https://www.frontiersin.org/articles/10.3389/fbioe.2019.00269/full#supplementary-material

Supplementary Table S1 | Muscle force data assigned to all finite element models for the major muscle of mastication, based on experimental data when the subject was chewing on nuts. The table shows the direction of the muscle action unit vector and estimated muscle force magnitude (rms EMG multiplied by the PCSA data × 30 kN/m²) for each muscle. Estimated muscle force was measured at the time of the maximum strain magnitude, measured from a gauge fixed to the labial surface of the inferior left mid-corpus (Panagiotopoulou et al., 2017).

Supplementary Table S2 | Raw in vivo experimental data when the subject was chewing on nuts (almond, cashew, brazil nut, pecan, walnut, seeds).

Supplementary Table S3 | Summary of differences in trabecular bone NO PDL and PDL models.

Supplementary Figure S1 | CT scan slices depicting segmentation of the PDL, with schematic representation of the Young’s Moduli assigned to the FEMs. In the PDL model the PDL is assigned Young’s Moduli ($E$) of 0.68 MPa, while in the NO PDL model the PDL is assigned $E$ value of 24,500 MPa (the same $E$ value assigned to the teeth).

Supplementary Figure S2 | Locations across the primate jaw where key differences between the PDL and NO PDL FEM were identified.
Supplementary Figure S3 | Scatter plot of maximum $\varepsilon_1$ (positive) and $\varepsilon_2$ (negative) strains (A) found at sample locations (B) in Models 1–4, where the PDL is assigned Young's Modulus (E) of 0.07, 0.18, 13.8, and 1,750 MPa, respectively.

Supplementary Figure S4 | Color plots of differences in maximum ($\varepsilon_1$) and minimum ($\varepsilon_2$) principal strain magnitudes in trabecular tissue between models that include (PDL Model) and exclude (NO PDL Model) the periodontal ligament. Pairs of FEMs are compared by mapping the surface distribution of element level differences in principal strains between the two models onto the cortical tissue surface of the model. Panels compare $\varepsilon_1$ and $\varepsilon_2$ magnitudes between the model pairs in four views. Scale bars to the right of each panel indicate the element level difference in principal strains ($\varepsilon_\mu$) between models. Areas of greater difference in results from PDL and NO PDL models are indicated by darker colors, while lighter colors indicate areas of high similarity.

Supplementary Figure S5 | Comparisons of principal strain magnitudes in cortical bone of FEM model pairs (PDL vs. NO PDL), where both left and right TMJs are constrained against translation in all directions. Pairs of FEMs are compared by mapping the differences in principal strains between the two models onto the cortical surface of the model. Each panel compares $\varepsilon_1$ and $\varepsilon_2$ magnitudes between the model pairs in three views. Scale bars to the right of each panel indicate the difference in principal strains ($\varepsilon_\mu$) between models. Areas of greater difference in results from PDL and NO PDL models are indicated by darker colors, while lighter colors indicate areas of high similarity.

Supplementary Figure S6 | Comparisons of principal strain magnitudes in cortical bone of FEM model pairs (PDL vs. NO PDL), where models were loaded with muscle activation scale factors used in Gröning et al. (2011). Pairs of FEMs are compared by mapping the differences in principal strains between the two models onto the cortical surface of the model. Each panel compares $\varepsilon_1$ and $\varepsilon_2$ magnitudes between the model pairs in three views. Scale bars to the right of each panel indicate the difference in principal strains ($\varepsilon_\mu$) between models. Areas of greater difference in results from PDL and NO PDL models are indicated by darker colors, while lighter colors indicate areas of high similarity.

Supplementary Figure S7 | Color distribution of $\varepsilon_1$ (maximum principal) strains of the whole FEM and trabecular tissue from PDL and NO PDL FEMs. Red and green ends of the scale represent higher and lower $\varepsilon_1$ concentrations, respectively.

Supplementary Figure S8 | Color distribution of $\varepsilon_2$ (minimum principal) strains of the whole FEM and trabecular tissue from PDL and NO PDL FEMs. Blue and green ends of the scale represent higher and lower $\varepsilon_1$ concentrations, respectively.

REFERENCES
Andersen, K. L., Mortensen, H. T., Pedersen, E. H., and Melsen, B. (1991a). Determination of stress levels and profiles in the periodontal ligament by means of an improved three-dimensional finite element model for various types of orthodontic and natural force systems. J. Biomed. Eng. 13, 293–303. doi:10.1016/0141-5425(91)90111-J
Andersen, K. L., Pedersen, E. H., and Melsen, B. (1991b). Material parameters and stress profiles within the periodontal ligament. Am. J. Orthod. Dentofacial Orthop. 99, 427–440. doi:10.1016/S0889-5406(05)81576-8
Berkovitz, B. K. (1990). The importance of craniofacial sutures in biomechanical finite element models of the domestic pig. PLoS ONE 7:e31769. doi:10.1371/journal.pone.0031769
Bright, J. A. (2012). The Importance of Craniofacial Sutures in Biomechanical Finite Element Models of the Domestic Pig. J. Dent. Res. 101, 261–266. doi:10.1177/0022034512444477
Cattaneo, P., Dalstra, M., and Melsen, B. (2005). The finite element method: a tool to study orthodontic tooth movement. J. Dent. Res. 84, 428–433. doi:10.1177/1540829X05084006
Cox, P. G., Fagan, M., Rayfield, E., and Jeffery, N. (2011). Finite element modelling of squirrel, guinea pig and rat skulls: using geometric morphometrics to assess sensitivity. J. Anat. 219, 696–709. doi:10.1111/j.1469-7580.2011.01408.x
Dechow, P. C., Panagiotopoulou, O., and Ghapare, P. (2017). Biomechanical implications of cortical elastic properties of the macaque mandible. Zoology124, 3–12. doi:10.1016/j.zool.2017.06.008
Dorow, C., Krstin, N., and Sander, F. G. (2003). Determination of the mechanical properties of the periodontal ligament in a uniaxial tensional experiment. J. Orofac. Orthop. 64, 100–107. doi:10.1007/s00056-003-0225-7
Dorow, C., Krstin, N., and Sander, F. G. (2014). Experiments to determine the material properties of the periodontal ligament. J. Orofac. Orthop. 63, 94–104. doi:10.1007/s00056-012-0117-4
Dumont, E. R., Grosse, I. R., and Slater, G. J. (2009). Requirements for comparing the performance of finite element models of biological structures. J. Theor. Biol. 256, 96–103. doi:10.1016/j.jtbi.2008.07.017
Dumont, E. R., Piccirillo, J., and Grosse, I. R. (2005). Finite-element analysis of biting behavior and bone stress in the facial skeletons of bats. Anat. Rec. A Discov. Mol. Cell. Evol. Biol. 283, 319–330. doi:10.1002/ar.a.20165
Goel, V. K., Khera, S. C., Gurusami, S., and Chen, R. C. (1992). Effect of cavity depth on stresses in a restored tooth. J. Prosthet. Dent. 67, 174–183. doi:10.1002/jpd.2990670406
Gröning, F., Fagan, M., and O'Higgins, P. (2011). The effects of modelling simplifications on craniofacial finite element models: the alveoli (tooth sockets) and periodontal ligaments (volume 44, issue 10, pages 1831–1838). J. Biomech. 45, 1749–1750; author reply 1750–1741. doi:10.1016/j.jbiomech.2011.10.042
Gröning, F., Fagan, M. J., and O'Higgins, P. (2011). The effects of the periodontal ligament on mandibular stiffness: a study combining finite element analysis and geometric morphometrics. J. Biomech. 44, 1304–1312. doi:10.1016/j.jbiomech.2011.01.008

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Grosse, I. R., Wood, S. A., Strait, D. S., Dumont, E. R., and Ross, C. F. (2012). Response to the comment by gröning and fagan on “The effects of modeling simplifications on craniofacial finite element models: the alveoli (tooth sockets) and periodontal ligaments” (volume 44, issue 10, pages 1831–1838). J. Biomech. 45, 1750–1751. doi: 10.1016/j.jbiomech.2012.01.047

Ho, S. P., Kuriya, M. P., Granfield, K., Huang, J., Herber, B. P., Ryder, M. L., et al. (2013). The plastic nature of the human bone-periodontal ligament-tooth fibrous joint. Bone 57, 455–467. doi: 10.1016/j.bone.2013.09.007

Hylander, W. L. (1979). The functional significance of primate mandibular form. J. Morphol. 160, 223–239. doi: 10.1002/jmor.1051600208

Hylander, W. L. (1984). Stress and strain in the mandibular symphysis of primates: a test of competing hypotheses. Am. J. Phys. Anthropol. 64, 1–46. doi: 10.1002/aja.1006401012

Hylander, W. L. (1985). Mandibular function and biomechanical stress and scaling. Am. Zool. 25, 315–330. doi: 10.1093/icb/25.2.315

Iriarte-Díaz, J., Reed, D. A., and Ross, C. F. (2011). Sources of variance in temporal and spatial aspects of jaw kinematics in two species of primates feeding on foods of different properties. Integr. Comp. Biol. 51, 307–319. doi: 10.1093/icb/icr072

Jeon, P. D., Turley, P. K., Moon, H. B., and Ting, K. (1999). Analysis of stress in the periodontium of the maxillary first molar with a three-dimensional finite element model. Am. J. Orthod. Dentofacial Orthop. 115, 267–274. doi: 10.1016/S0889-5406(99)70328-8

Kelling, L., Drönhagen, M., Tran, K. L., Hasan, I., Reimann, S., Deschner, J., et al. (2016). In vivo measurements and numerical analysis of the biomechanical characteristics of human periodontal ligament. Ann. Anat. 206, 80–88. doi: 10.1016/j.aanat.2015.08.004

Korioth, T., and Hannam, A. (1994). Deformation of the human mandible during simulated tooth clenching. J. Dent. Res. 73, 56–66. doi: 10.1177/00220345970730010801

Korioth, T. W., Romilly, D. P., and Hannam, A. G. (1992). Three-dimensional finite element stress analysis of the dentate human mandible. Am. J. Phys. Anthropol. 88, 69–96. doi: 10.1002/aja.100880107

Kucziuk, C., Dobson, C. A., Crompton, R. H., Phillips, R., Oxnard, C. E., Fagan, M. J., et al. (2009). Masticatory loading and bone adaptation in the supraorbital torus of developing macaques. Am. J. Phys. Anthropol. 139, 193–203. doi: 10.1002/anaat.200972

Li, L. W., Wang, Z. Y., Bai, Z. C., Mao, Y., Gao, B., Xin, H. T., et al. (2006). Three-dimensional finite element analysis of weakened roots restored with different cements in combination with titanium alloy posts. Chin. Med. J. 119, 305–311. doi: 10.1007/s00223-006-02020-00007

Marinescu, R., Daegling, D. J., and Rapoff, A. J. (2005). Finite-element modeling of the anthropoid mandible: the effects of altered boundary conditions. Anat. Rec. A Discov. Mol. Cell. Evol. Biol. 283, 300–309. doi: 10.1002/ar.20166

McCormack, S. W., Witzel, U., Watson, P. J., Fagan, M. J., and Gröning, F. (2014). The biomechanical function of periodontal ligament fibres in orthodontic tooth movement. PLoS ONE 9:e102387. doi: 10.1371/journal.pone.0102387

McCormack, S. W., Witzel, U., Watson, P. J., Fagan, M. J., and Gröning, F. (2017). Inclusion of periodontal ligament fibres in mandibular finite element model. Bone 57, 1–10. doi: 10.1016/j.bone.2016.03.00005-5

Qian, L., Todo, M., Morita, Y., Matsuhashi, Y., and Koyano, K. (2009). Deformation analysis of the periodontium considering the viscoelasticity of the periodontal ligament. J. Periodont. 25, 1285–1292. doi: 10.1002/j.1600-0765.2009.00314

Rees, J. S. (2001). An investigation into the importance of the periodontal ligament and alveolar bone as supporting structures in finite element studies. J. Oral Rehabil. 28, 425–432. doi: 10.1034/j.1365-2842.2001.00686.x

Reinhardt, R. A., Pao, Y. C., and Krejci, R. F. (1984). Periodontal ligament stresses in the initiation of occlusal traumatism. J. Periodont. Res. 19, 238–246. doi: 10.1111/j.1600-0765.1984.tb00815.x

Ren, L. M., Wang, W. X., Takao, Y., and Chen, Z. X. (2010). Evaluation of the biomechanical characteristic of tooth supporting structure under occlusal load. J. Jpn Soc. Powder Powder Metall. 57, 298–305. doi: 10.2497/jspm.57.298

Ross, C. F., Iriarte-Díaz, J., and Nunn, C. L. (2012). Innovative approaches to the relationship between diet and mandibular morphology in primates. Int. J. Primatol. 33, 632–660. doi: 10.1007/s10764-012-9559-y

Sadak, S., and Kamio, E. (1971). Receptive fields and directional sensitivity of single sensory units innervating the periodontal ligaments of the cat mandibular teeth. Bull. Tokyo Dent. Coll. 12, 25–43.

Sandino, C., McErlain, D. D., Schipilow, J., and Boyd, S. K. (2015). The viscoelastic properties of trabecular bone: a micro computed tomography-based finite element study J. Mech. Behav. Biomed. Mater. 44, 1–9. doi: 10.1016/j.jmbbm.2014.12.018

Sinclair, A. G., and Alexander, R. M. (1987). Estimates of forces exerted by the jaw muscles of some reptiles. J. Zool. 213, 107–115. doi: 10.1111/j.1469-7998.1987.tb35610.x

Slater, G. J., Dumont, E. R., and Van Valkenburgh, B. (2009). Implications of predatory specialization for cranial form and function in canids. J. Zool. 278, 181–188. doi: 10.1111/j.1469-7998.2009.00567.x

Slater, G. J., Figueirido, B., Louis, L. Yang, P., and Van Valkenburgh, B. (2010). Biomechanical consequences of rapid evolution in the polar bear lineage. PLoS ONE 5:e13870. doi: 10.1371/journal.pone.0013870

Natali, A. N., Pavan, P. G., and Scarpa, C. (2004). Numerical analysis of tooth mobility: formulation of a non-linear constitutive law for the periodontal ligament. Dent. Mater. 20, 623–629. doi: 10.1016/j.dental.2003.08.003

Nelson, G. J. (1986). Three Dimensional Computer Modeling of Human Mandibular Biomechanics. Vancouver, BC: University of British Columbia.
Smith, A. L., Benazzi, S., Ledogar, J., A., Tamvada, K., Pryor Smith, L. C., Weber, G. W. (2015a). The feeding biomechanics and dietary ecology of Paranthropus boisei. Anat. Rec. 298, 145–167. doi: 10.1002/ar.23073

Smith, A. L., Benazzi, S., Ledogar, J., A., Tamvada, K., Smith, L. C. P., Weber, G. W. (2015b). Biomechanical implications of intraspecific shape variation in chimpanzee crania: moving towards an integration of geometric morphometrics and finite element analysis. Anat. Rec. 298, 122–144. doi: 10.1002/ar.23074

Strait, D. S., Richmond, B. G., Spencer, M. A., Ross, C. F., Dechow, P. C., and Wood, B. A. (2007). Masticatory biomechanics and its relevance to early hominin phylogeny: an examination of palatal thickness using finite-element analysis. J. Hum. Evol. 52, 585–599. doi: 10.1016/j.jhevol.2006.11.019

Strait, D. S., Wang, Q., Dechow, P. C., Ross, C. F., Richmond, B. G., Spencer, M. A., et al. (2005). Modeling elastic properties in finite-element analysis: how much precision is needed to produce an accurate model? Anat. Rec. A Discov. Mol. Cell. Evol. Biol. 283, 275–287. doi: 10.1002/ar.20172

Strait, D. S., Weber, G. W., Neubauer, S., Chalk, J., Richmond, B. G., Lucas, P. W., et al. (2009). The feeding biomechanics and dietary ecology of Australopithecus africanus. Proc. Natl Acad. Sci. U.S.A. 106, 2124–2129. doi: 10.1073/pnas.0808730106

Takahashi, N., Kitagami, T., and Komori, T. (1980). Behaviour of teeth under various loading conditions with finite element method. J. Oral Rehabil. 7, 453–461. doi: 10.1111/j.1365-2842.1980.tb00464.x

Thresher, R. W., and Saito, G. E. (1973). The stress analysis of human teeth. J. Biomech. 6, 443–449. doi: 10.1016/0021-9290(73)9003-1

Toro-Ibacache, V., Fitton, L. C., Fagan, M. J., and O’Higgins, P. (2016). The effect of varying jaw-elevator muscle forces on a finite element model of a human cranium. Anat. Rec. 299, 828–839. doi: 10.1002/ar.23358

Trulsson, M., Johansson, R., S., and Olsson, K. A. (1992). Directional sensitivity of human periodontal mechanoreceptive afferents to forces applied to the teeth. J. Physiol. 447, 373–389. doi: 10.1113/physiol.1992.sp019007

Van Driel, W., Van Leeuwen, E., Von den Hoff, J., Maltha, J., and Kuipers-Jagtman, A. (2000). Time-dependent mechanical behaviour of the periodontal ligament. Proc. Ins. Mech. Eng. H 214, 497–504. doi: 10.1243/0954411001535525

van Eijden, T. M. G. J., Koolstra, J. H., and Brugman, P. (1995). Architecture of the human pterygoid muscles. J. Dent. Res. 74, 1489–1495. doi: 10.1777/00220345950740080901

van Eijden, T. M. G. J., Koolstra, J. H., and Brugman, P. (1996). Three-dimensional structure of the human temporalis muscle. Anat. Rec. 246, 565–572. doi: 10.1002/(SICI)1097-0185(199612)246:4<565::AID-AR17>3.0.CO;2-M

Wang, C. Y., Su, M. Z., Chang, H. H., Chiang, Y. C., Tao, S. H., Cheng, J. H., et al. (2012). Tension-compression viscoelastic behaviors of the periodontal ligament. J. Formos. Med. Assoc. 111, 471–481. doi: 10.1016/j.jfma.201 1.06.009

Wills, D. J., Picton, D. C. A., and Davies, W. I. R. (1976). A study of the fluid systems of the periodontium in macaque monkeys. Arch. Oral Biol. 21, 175–185. doi: 10.1016/0003-9969(76)90127-8

Wood, S. A., Strait, D. S., Dumont, E. R., Ross, C. F., and Grosse, I. R. (2011). The effects of modeling simplifications on craniofacial finite element models: the alveoli (tooth sockets) and periodontal ligaments. J. Biomech. 44, 1831–1838. doi: 10.1016/j.jbiomech.2011.03.022

Wroe, S., Moreno, K., Claussen, P., McHenry, C., and Curnoe, D. (2007). High-resolution three-dimensional computer simulation of hominin cranial mechanics. Anat. Rec. 290, 1248–1255. doi: 10.1002/ar.20594

Yettram, A., Wright, K., and Houston, W. (1977). Centre of rotation of a maxillary central incisor under orthodontic loading. Br. J. Orthod. 4, 23–27. doi: 10.1179/bjo.4.1.23

Zhang, Y. R., Du, W., Zhou, X. D., and Yu, H. Y. (2014). Review of research on the mechanical properties of the human tooth. Int. J. Oral Sci. 6, 61–69. doi: 10.1038/ijos.2014.21

Conflict of Interest: The authors declare that the research was conducted in the absence of any commercial or financial relationships that could be construed as a potential conflict of interest.

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