X-ray ptychographic computed tomography at 16 nm isotropic 3D resolution

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X-ray ptychography is a scanning variant of coherent diffractive imaging with the ability to image large fields of view at high resolution. It further allows imaging of non-isolated specimens and can produce quantitative mapping of the electron density distribution in 3D when combined with computed tomography. The method does not require imaging lenses, which makes it dose efficient and suitable to multi-keV X-rays, where efficient photon counting, pixelated detectors are available. Here we present the first highly resolved quantitative X-ray ptychographic tomography of an extended object yielding 16 nm isotropic 3D resolution recorded at 2 Å wavelength. This first-of-its-kind demonstration paves the way for ptychographic X-ray tomography to become a promising method for X-ray imaging of representative sample volumes at unmatched resolution, opening tremendous potential for characterizing samples in materials science and biology by filling the resolution gap between electron microscopy and other X-ray imaging techniques.

Computed tomography provides valuable information to materials science, biology, and physics in a non-destructive way that is amenable to complementary tests during or after the measurement. Multi-keV X-rays provide a penetration depth allowing tomography of large and thus representative sample volumes. In the past few years, coherent diffractive imaging (CDI) has been established as one way to overcome limiting factors in resolution, such as X-ray imaging optics, which are replaced by phase retrieval algorithms1–4. A particularly robust modality of CDI is ptychography, where a sample is scanned in two dimensions perpendicular to a spatially confined coherent X-ray beam, and at each position a coherent diffraction pattern of the transmitted radiation is recorded5. Redundant information from overlapping illuminated areas significantly adds robustness and improves convergence of the iterative image reconstruction algorithms. This technique allows imaging of arbitrarily extended objects in 2D, and by recording several 2D projections of a sample at different orientations with respect to the X-ray beam, quantitative 3D images of the electron density of large objects can be obtained6,7. The instrumentation related to high-resolution X-ray tomography is demanding and many developments are pursued and implemented worldwide8–11. The achievable resolution in ptychography is determined by the scanning positioning accuracy, the stability of the whole measurement system and by the angular extent of the X-ray scattering of the sample that can be measured with a sufficient signal-to-noise ratio, which in turn is determined by sample composition, exposure time and the detection system. Given this, there is a strong potential for X-ray ptychographic tomography to reach unmatched resolution while imaging representative sample volumes. Here we present the first experimental demonstration reaching an isotropic 3D resolution of 16 nm.

Results
Prior to an evaluation of the 3D capabilities of ptychography it is useful to assess resolution in 2D, where ptychography has demonstrated to reach the 10 nm resolution range12–14. Resolution tests of 2D samples at different tomographic orientations help to identify and diagnose problems or limitations of the tomography system. Our measurements were carried out at the cSAXS beamline at the Paul Scherrer Institut, Switzerland, using an instrument based on that described in Ref. 15 and schematically shown in Fig. 1. Significant modifications to this setup were instrumental for the improved performance and are described in the Methods Section and Supplementary Method 2. The position and positioning stability of the sample is measured interferometrically with respect to the beam defining optics, yielding a precision (average standard deviation) of 12.1 nm during
Figure 1 | Tomography setup, composed of X-ray optics and sample stage units. The optics stage contains a central stop (CS), a Fresnel zone plate (FZP) and an order-sorting aperture (OSA) for conditioning the X-ray beam. The sample stage performs the 2D scans and allows a rotation \( \theta_x \) around the y-axis for tomography. The relative position of sample and optics \( \Delta x \) and \( \Delta y \), as well as the wobble angle of the sample stage \( \theta_y \), is measured via optical interferometry.

Detector exposures. Ptychographic measurements of a 2D Siemens star test pattern were performed at 6.2 keV photon energy using a beam diameter of 700 nm. Far-field diffraction patterns were recorded with a Pilatus 2M detector\(^{16,17} \) at a distance of 2.363 meters and the reconstructions were performed to a real-space pixel size of 6.9 nm. Details on the 2D sample, its measurement and the reconstructions can be found in the Supplementary Method 1.

As an initial evaluation of the instrument performance, three independent measurements of the same \( 2 \times 2 \mu m^2 \) area of the sample were recorded at different tomographic orientations \( \theta_y \), i.e. at different rotation angles around the y-axis as defined in Fig. 1. Specifically, two images at \( \theta_y = 0^\circ \) and one at \( \theta_y = 180^\circ \) were acquired. For the comparison of the results, the image at \( \theta_y = 180^\circ \) was mirrored about its vertical axis. In Fig. 2(a) we show the phase of the ptychographic reconstruction of the sample at \( \theta_y = 0^\circ \), revealing the projected density of the object along the X-ray propagation direction. After subpixel image registration\(^{18} \), the resolution and repeatability of the measurement was evaluated from a pair of independent measurements using Fourier shell correlation (FSC). For this a correlation curve in Fourier domain is obtained between the two images and theemens using Fourier shell correlation (FSC). For this a correlation measurement was evaluated from a pair of independent measurements of the same 2D test pattern. (b) Resolution estimation of the image in (a) by Fourier shell correlation with an independently measured image recorded at \( \theta_y = 0^\circ \) and \( \theta_y = 180^\circ \), respectively. Because we estimate here the resolution of the individual images rather than their average, we use the 1-bit threshold criterion.

While two dimensional test objects are useful for characterizing the resolution that can be achieved in an individual 2D projection of a tomography method, such measures do not necessarily correspond to achievable 3D resolution. This is because such 2D resolution tests or even tomography data of a 2D sample measured over a limited angular range do not include characterization of effects such as a wobble motion of the axis of rotation, angular error motions of scan stages, thermal drifts, misalignments or depth of focus in a thick object. A true measure of 3D resolution requires a 3D test object that provides small and sharp features, yet having curved interfaces to avoid X-ray reflections and tomographic reconstruction artifacts from extended flat surfaces. A 3D test sample should provide a well-characterized complex-structure, strong X-ray interaction and be resistant to radiation damage. Here we developed a sample based on a porous SiO\(_2\) structure of 139 nm mean pore size that was later coated by a Ta\(_2\)O\(_5\) layer of 37 nm thickness. The sample was further milled in a quasi cylindrical shape to a size of about 6 \( \mu m \) diameter, for further details see “3D sample preparation” in the Methods. The field of view of the 2D projections acquired for this sample was 9 \( \times \) 3 \( \mu m^2 \). In total, four sub-tomograms of 180 projections each were recorded sequentially at interleaved angles, resulting in a total of 720 projections taken with equal angular spacing and spanning a range from \( \theta_y = 0^\circ \) to \( \theta_y = 180^\circ \). The reconstructions of the projections, one of them shown in Fig. 3, were performed to a real-space pixel size of 10 nm and a tomogram was then computed from the phase reconstructions, providing a 3D map of the density of the object. For details see “Data acquisition and tomographic reconstruction” in the Methods. A cross section of this tomogram is depicted in Fig. 4(a) and a zoom in Fig. 4(b) where we can clearly observe the base porous structure and the thin Ta\(_2\)O\(_5\) layer surrounding the pore structure. Figure 4(a) is complemented by supplementary movie 1, giving an overview of the sample.

To estimate the tomogram resolution, the full data set of 720 projections was divided in half and two independent tomograms with double angular spacing and consequently half the number of projections were reconstructed. Figure 4(d) shows the FSC curve...
between these independent 3D reconstructions and gives a half-period resolution estimate of 15.9 nm where the $K_{\text{bit}}$ threshold curve intersects the FSC. The determined 3D resolution is supported by line cuts, as shown in Fig. 4(c). Table 1 shows a comparison between the resolution we obtained by the FSC half-bit criterion and the resolution limit defined by Nyquist angular sampling, given by $(\pi/2) \times$ sample thickness/#projections, when taking a different number of projections into account. As expected, the resolution continuously improves when adding projections to the tomogram and our measured resolution is close to the expected resolution. The reconstructed pixel size of 10 nm was not limiting our tomographic resolution, as confirmed by a reconstruction performed to a pixel size of 6.9 nm. The FSC intersects the threshold value of 0.5, which is often used in electron microscopy, at 18.4 nm. Since there are many ways of defining resolution, we provide an extracted sub-volume of the tomogram as tiff-stack as supplementary dataset 1. This volume is also represented in supplementary movie 2 with an identical color scale as used in Fig. 4(a).

In the tomographic slice in Fig. 4(a) three distinct gray levels are visible for air (black), glass (gray), and a thin layer of Ta$_2$O$_5$ (white). The porous glass structures are conformally coated by Ta$_2$O$_5$ atomic layer deposition (ALD), and a gradient of the Ta$_2$O$_5$ layer thickness can be observed due to the limited diffusion of the precursor into the porous structure$^{20,21}$. The sample cylinder is surrounded by material with different density values, as observed at either side of the sample in Fig. 4(a), arising from material redeposition during sample preparation using focused ion beam milling. Electron density can be converted to mass density when the chemical composition of the sample is known and the measurement is taken away from absorption edges of the sample materials$^7$. As an example, we measured a glass density of 2.1 g/cm$^3$ with a standard deviation of 0.5 g/cm$^3$, obtained from the peak in the histogram taken from a volume within the tomogram of about (2 µm)$^3$. This value agrees with the documented average density of the material$^{22}$ of 2.20 g/cm$^3$.

**Discussion**

Our measurements on the 2D test object show a similar FSC at identical and 180 degree complementary projection angles $\theta$. This proves the correct alignment of detector pixels with respect to the tomography axis and that image deformations and distortions caused by the instrumentation, for instance by sample mispositioning, occur on a smaller length scale. The FSC is a measure of signal-to-noise ratio, and in Fig. 2(b) it shows a very high repeatability at low spatial frequencies and a sharp transition to the low-SNR regime near the cutoff. When specifying the resolution of a tomography instrument, such correlation information of both identical and complementary 180 degrees projection angles provides important information on the instrument performance that cannot be adequately assessed by the quality obtained at a single projection angle which may be subject to systematic errors and not be representative of the 3D imaging capabilities. It is also a fast verification method of the instrument performance and therefore is a good routine check prior tomographic data acquisition.

**Figure 3** | Reconstructed 2D projection of the 3D test object prior to the tomographic reconstruction showing phase (a) and amplitude (b).

**Figure 4** | Results of the tomographic reconstruction. (a) Section of the tomogram parallel to the rotation axis. Three distinct gray levels are visible for air (black), glass (gray), and a thin layer of Ta$_2$O$_5$ (white) conformal to the pores. (b) Zoom in of a region indicated by the yellow rectangle in (a). (c) Line profile indicated by a red line in (a) and (b) showing 16.4 nm edge response using the 10%-90% criteria. (d) Resolution estimation by Fourier shell correlation (FSC) computed using all 720 projections.
The interferometrically measured stability of our setup of 12.1 nm during exposures is in agreement with our estimated resolution on the 2D sample. Although it may be difficult to quantify we found no evidence of image degradation caused by this intra-exposure jitter and we found this to be the limiting factor for the obtained 2D resolution, meaning that increasing the exposure time did not lead to a resolution better than 10 nm. The averaged relative positions between sample and X-ray optics of each detector exposure are directly used in the ptychography reconstructions, which compensates low-frequency instabilities such as thermal drift, and makes algorithm refinement of scanning positions unnecessary. This is an important property of our instrument as position refinement is ultimately limited by sample contrast and may have unsatisfactory performance on weakly scattering specimens such as biological material.

The tomogram resolution continuously improves when adding projections to the tomogram. For the FSC, the tomograms to compare are obtained from half the number of projections. Because these measurements are limited by angular sampling, their correlation at high spatial frequencies is diminished which makes the FSC estimate conservative. On the other hand, the Nyquist angular sampling can be too stringent for realistic samples. While, potentially, the full tomogram of 720 projections could have higher resolution, the determined 3D resolution is supported by line cuts, as shown in Fig. 4(c), and is in good agreement with the 2D projection resolution of 15.5 nm, determined using the FSC 1 bit criterion\(^19\) between two projections at the same rotation angle before and after the tomographic measurement.

The tomographic resolution is still worse than that obtained on the flat 2D sample, which is partially attributed to radiation damage induced in the 3D sample during the measurement. Radiation damage was assessed by FSC of individual projections taken at the same angle \(\theta_0 = 0^\circ\) before, in the middle, and after recording the tomogram. For two projections prior to the tomographic measurement we obtain a 2D resolution estimate of 13.4 nm using the 1 bit criterion. When comparing a projection from the beginning with one recorded in the middle of the tomogram we determine a slight decrease to 14.1 nm, and a comparison of a projection from the beginning with a projection from after the tomogram results in a further decrease to 15.5 nm. This motivates our conclusion that radiation damage limited our resolution to around 16 nm. Another possible limiting factor for resolution is the sample thickness which affects both CDI and ptychography\(^19,20\). We have investigated this issue through numerical simulations characterizing the effect of sample thickness on the width of the point spread function (PSF), which ultimately can be used to estimate resolution. From these simulations we conclude that, although the shape and sidelobe intensity of the PSF changes, its width is preserved to 16 nm for a sample up to 7 microns in thickness. Further discussion can be found in the Supplementary Method 3.

The estimated total dose deposited in the material during the measurement of 720 projections was \(720\times1.2\times10^{10}\) Gray. As an attempt to test the instrumentation limits, the dose was not minimized in the measurement. On a 2D projection we found that a fourfold reduction of exposure time produces results with identical resolution, which gives us confidence that a dose of \(3 \times 10^9\) Gray would have sufficed for the entire tomogram at the achieved 3D resolution of 16 nm. Cleary such dose is relatively high but when compared with previous measurements\(^6\) it is also expected as the required dose for imaging scales with resolution to the forth power\(^20\).

We demonstrated that ptychographic tomography is a promising technique that combines imaging of representative sample volumes with high resolution by combining coherent diffractive imaging and a scanning approach, thereby closing the resolution gap between electron microscopy and X-ray imaging techniques. Although our demonstration was performed on an artificial test sample with enhanced contrast via heavy atom deposition, its complexity is comparable to realistic materials such that this demonstration paves the way to accurate analysis of representative sample volumes in materials science or even life science samples. However, it also shows that even on radiation tolerant samples like our nanoporous glass, damage already plays a role and limits resolution. To reach a 3D resolution towards 10 nm, cryogenic sample preservation will become mandatory for most sample materials and efforts are underway to achieve this.

### Methods

#### Instrumentation.
The tomography setup, depicted in Fig. 1, is based on the instrument described in Ref. 15, where significant modifications were implemented to drastically improve the 3D resolution. The instrument consists of two mechanical units. Firstly, a sample stage allows precise movements for scanning the sample through the beam and is equipped with a rotation axis for tomography. Secondly, an optics stage for the optical elements is used to define the beam illuminating the sample. The sample measurements we use a diffractive X-ray lens, a Fresnel zone plate, with 100 nm diameter and an outermost zone width of 100 nm to define the illumination incident on the sample. Differential laser interferometry is used to measure the relative positions (\(\Delta x, \Delta y\)) between the X-ray optics and sample and to close the mechanical loop ensuring accurate and stable sample positioning. A further interferometer measures the angular error motion \(\theta\) of the scanning mechanism. Using positions (\(\Delta x\), \(\Delta y\)) and angular measurement \(\theta\), a corrected sample position was calculated and directly used in the ptychographic reconstructions. Further details can be found in the Supplementary Method 2.

#### 3D sample preparation.
The tomography sample is based on nanoporous glass with a mean pore size of 139 nm, which is intended for use in the calibration of high pressure mercury porosimeters. As a reference material it has the advantage of being already well characterized by several methods\(^2\). A TaO\(_3\) film was fabricated on the surface of this glass material by atomic layer deposition from Ta(OC\(_2\)H\(_5\))\(_5\) and H\(_2\)O at 250 °C using a SUNALE reactor (Picosun Oy, Finland)\(^19\). The final film thickness was 37 nm in the outermost region of the glass beads. Using a focused ion beam, a cylinder of 6 microns diameter of this material was milled and mounted on a sample holder. This sample allows tomographic data to be taken at any projection angle without missing wedge, providing isotropic 3D resolution. It is ideal for evaluating the performance of high-resolution X-ray tomography instrumentation as it is radiation tolerant, and it provides features of 37 nm and 139 nm that are well distributed in their three-dimensional position and orientation at two distinct high-contrast levels.

#### Data acquisition and tomographic reconstruction.
A tomogram of the 3D sample was recorded using ptychographic tomography. As mentioned previously, 720 projections were recorded with equal angular spacing and spanning a range of \(0^\circ\) to \(\theta_0 = 180^\circ\), divided in four sequentially recorded sub-tomograms, each consisting of 180 projections. Each projection was acquired using a ptychographic scan of 343 exposures arranged in concentric circles with 250 nm radial step size, covering an area of \(9 \times 3 \mu\text{m}^2\) with an exposure time of 0.6 s per point and a beam diameter of 600 nm. Ptychographic measurements were performed at 6.2 keV photon energy, and the diffraction patterns were recorded with a Pilatus 2M detector with a pixel size of 172 \(\mu\text{m}\)\(^2\) at a distance of 2.363 m. Including sample positioning and detector readout, the measurement of each projection took about 280 s. Of the diffraction patterns a region of 270 \(\times\) 270 pixels was used in the reconstructions, resulting in a pixel size of 10 nm.

Reconstructions were performed by sharing information between consecutive scans taken at different projection angles. To measure information lost in the gaps between Pilatus modules, the detector is moved transversely to the direction of X-ray propagation. In previous work, akin to the measurements on the 2D sample, the measurement of each projection was repeated at each detector position and reconstructions were performed from the pair of measurements with suitable validation\(^14\). However, repeating the scan for each projection caused a significant overhead. For this work a scan on each tomography angle is performed only once while the detector position is alternated, and for two successive scans the illumination is enforced to be

| Number of projections | Isotropic 3D resolution [nm] | Expected 2D resolution [nm] |
|-----------------------|-----------------------------|----------------------------|
| 180                   | 58.5                        | 50                         |
| 360                   | 30.0                        | 25                         |
| 720                   | 15.9                        | 12.5                       |

Table 1 | Estimated resolution of the tomograms reconstructed with different numbers of projections and expected resolution according to Nyquist angular sampling. The FSC analysis was based on the half-bit criterion and was performed by processing two independent tomograms with double angular spacing.
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