MID-INFRARED GALAXY LUMINOSITY FUNCTIONS FROM THE AGN AND GALAXY EVOLUTION SURVEY

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ABSTRACT

We present galaxy luminosity functions at 3.6, 4.5, 5.8, and 8.0 μm measured by combining photometry from the IRAC Shallow Survey with redshifts from the AGN and Galaxy Evolution Survey (AGES) of the NOAO Deep Wide-Field Survey Boötes field. The well defined IRAC samples contain 3800–5800 galaxies for the 3.6–8.0 μm bands with spectroscopic redshifts and z < 0.6. We obtained relatively complete luminosity functions in the local redshift bin of z < 0.2 for all four IRAC channels that are well fitted by Schechter functions. After analyzing the samples for the whole redshift range, we found significant evolution in the luminosity functions for all four IRAC channels that can be fitted as an evolution in $M_\ast$ with redshift, $\Delta M_\ast = Qz$. While we measured $Q = 1.2 \pm 0.4$ and $1.1 \pm 0.4$ in the 3.6 and 4.5 μm bands consistent with the predictions from a passively evolving population, we obtained $Q = 1.8 \pm 1.1$ in the 8.0 μm band consistent with other evolving star formation rate estimates. We compared our luminosity functions with the predictions of semi-analytical galaxy formation and found the best agreement at 3.6 and 4.5 μm, rough agreement at 8.0 μm, and a large mismatch at 5.8 μm. These models also predicted a comparable $Q$-value to our luminosity functions at 8.0 μm, but predicted smaller values at 3.6 and 4.5 μm. We also measured the luminosity functions separately for early- and late-type galaxies. While the luminosity functions of late-type galaxies resemble those for the total population, the luminosity functions of early-type galaxies in the 3.6 and 4.5 μm bands indicate deviations from the passive evolution model, especially from the measured flat luminosity density evolution. Combining our estimates with other measurements in the literature, we found 53 ± 18% of the present stellar mass of early-type galaxies was assembled at $z = 0.7$.

Key words: galaxies: evolution – galaxies: luminosity function, mass function

Online-only material: color figures, machine-readable table

1. INTRODUCTION

The luminosity functions (LFs) of galaxies provide fundamental clues to the evolution of galaxies. Until recently, measurements of the galaxy LFs were largely confined to near-infrared (near-IR) to UV wavelengths (e.g., Blanton et al. 2003; Brown et al. 2007; Faber et al. 2007; Cirasuolo et al. 2007 for recent results) mainly due to the observational difficulties of covering large areas in the mid-infrared (mid-IR). The early mid/far-infrared (far-IR) studies of galaxies utilized the IRAS, ISO, and COBE satellites and ground-based submillimeter observations. These early studies led to the discovery of strong far-IR background radiation (Puget et al. 1996; Hauser et al. 1998; Fixsen et al. 1998), understanding the properties of luminous and ultra-luminous IR galaxies (e.g., Soifer et al. 1987; Sanders & Mirabel 1996; Barger et al. 1999), and earlier measurements of LFs in the mid/far-IR bands (e.g., Soifer et al. 1987; Rowan-Robinson et al. 1987; Saunders et al. 1990; Xu et al. 1998). The Spitzer Space Telescope (Werner et al. 2004), with its unprecedented capabilities, allows us to significantly expand on these results. In particular, the Spitzer/IRAC Channels 1–4 cover wavelengths of 3.6, 4.5, 5.8, and 8.0 μm (Fazio et al. 2004), respectively, providing unique windows for studies of galaxy properties. At low redshifts ($z \lesssim 1$), the 3.6 μm and 4.5 μm channels lie on the Rayleigh–Jeans tail of the black-body spectrum of stars, directly tracing the stellar mass with little sensitivity to the interstellar medium (ISM) either through absorption or emission. The 8.0 μm channel contains polycyclic aromatic hydrocarbon (PAH) features whose luminosity is well correlated with star formation rates. The situation for the 5.8 μm channel is more complicated since the galaxy flux is composed of a mixture of starlight and PAH features. Overall, the Spitzer/IRAC channels provide a comprehensive view of galaxy physics in the mid-IR.

Recently, several studies have measured luminosity functions in the near- and mid-IR based on IRAC photometry in the Chandra Deep Field South, Hubble Deep Field North, Great Observatories Origins Deep Survey, COMBO-17, and Spitzer Wide-Area Infrared Extra-galactic (SWIRE) surveys, where the majority of the galaxy redshifts are photometric redshifts, complemented by spectroscopic redshifts from these surveys and the VIMOS VLT Deep Survey (VVDS; Le Fèvre et al. 2005). In particular, there are studies using 2600 24 μm sources with 1941 spectroscopic redshifts (Le Floc’h et al. 2005), 8000 24 μm sources with photometric redshifts (Pérez-González et al. 2005), 1478 3.6 μm sources with 47% spectroscopic redshifts (Franceschini et al. 2006), 1349 24 μm sources with photometric redshifts (Caputi et al. 2007), 17,300–88,600 3.6–24 μm sources with photometric redshifts (WISE; Babbedge et al. 2006), and 21,200 3.6 μm sources with 1500 spectroscopic redshifts.
(Arnouts et al. 2007). Most of these studies use a combination of several photometric and redshift surveys. Semi-analytical models of galaxy evolution have also been developed to provide theoretical basis for comparisons to the observed LFs (e.g., models of galaxy evolution have also been developed to provide of several photometric and redshift surveys. Semi-analytical (Arnouts et al. 2007). Most of these studies use a combination of statistical and systematic uncertainties. The situation is further complicated by the presence of cosmic variance both within and between surveys and the heavy dependence on photometric redshifts. While photometric redshifts are frequently necessary for achieving a large sample size or a longer luminosity baseline, they can also lead to systematic uncertainties in the shape and evolution of the luminosity functions. Moreover, as we find in this study, the redshift dependence of the definition of luminosity can be a problem for estimates of evolution rates.

In this paper, we present mid-IR galaxy luminosity functions for $z < 0.6$ in the Spitzer/IRAC bands by combining the IRAC Shallow Survey (Eisenhardt et al. 2004) of the NOAO Deep Wide-Field Survey (NDWFS; Jannuzi & Dey 1999) with redshifts from the AGN and Galaxy Evolution Survey (AGES; C. S. Kochanek et al. 2009, in preparation). For the 3.6–8.0 μm IRAC bands we have well defined samples with roughly 3800–5800 spectroscopic redshifts and a statistical power corresponding to samples of 4600–8000 objects through the use of random sparse sampling. We describe the sample selection, photometry, and redshifts in Section 2, the LF measurement methods in Section 3, and the LFs in Section 4. We discuss our results in Section 5. We assume that $H_0 = 100 \, h \, \text{km} \, \text{s}^{-1} \, \text{Mpc}^{-1}$, $\Omega_m = 0.3$, and $\Omega_k = 0.7$, and use the Vega magnitude system throughout the paper.

### 2. SAMPLE SELECTION

We measured the mid-IR galaxy LFs in the NDWFS Boötes field by combining IRAC photometry from the IRAC Shallow Survey and AGES redshifts. This field is also covered by multiwavelength data in the UV (GALEX; Martin et al. 2005), optical (NDWFS), z-band (zBoötes; Cool 2007), near-IR (NDWFS and FLAMEX; Elston et al. 2006), and far-IR (24 μm; Soifer et al. 2004), allowing us to use spectral energy distribution (SED) models to type the galaxies and make K-corrections (Section 2.1). For simplicity, we briefly discuss the IRAC photometry and leave the discussion of photometry in the other bands to the references for each survey.

The IRAC Shallow Survey imaged the NDWFS field to 5σ limits of 18.4 (17.3), 17.7 (15.4), 15.5 (76) and 14.8 (76) mag (μJy) at [3.6]–[8.0] respectively for a 6′′ diameter aperture (Eisenhardt et al. 2004). We used the IRAC Shallow Survey SExtractor® MAGAUTO (similar to Kron magnitudes) and 6′′ aperture magnitudes for our analysis. We note that the 6′′ aperture magnitudes include point-spread function (PSF) corrections for flux losses outside the aperture. Galaxies were selected as extended sources in the NDWFS optical data. We were concerned about the reliability of the total (from MAGAUTO) mid-IR magnitudes since MAGAUTO may underestimate the total flux for extended galaxies by using a photometric aperture that is too small (e.g., Graham & Driver 2005; Brown et al. 2007). The problems can occur when the field is crowded with many sources or the exposure is relatively shallow, and will result in galaxy-size-dependent corrections that may mimic redshift evolution (see Appendix A). Since the optical bands have deeper images of the field with better PSFs, and the fixed aperture magnitudes do not suffer from this issue, we calculated total − 6′′ aperture magnitudes in the optical and in the IRAC bands to test whether the IRAC photometry showed signs of such a problem. We found a difference of 0.15 mag between the total − 6′′ aperture magnitudes in the optical and IRAC bands over the redshift range from 0 to 0.5. In particular, at low redshift ($z = 0$) the IRAC aperture correction is smaller than the optical bands. Since we view the optical correction as more reliable, due to the higher resolution and greater relative depth of the data at these redshifts, we define the total magnitudes as the IRAC 6′′ aperture magnitude corrected by the $R$-band total to 6′′ aperture correction,

$$m_{\text{IRAC,total}} \equiv m_{\text{IRAC,6''}} + m_{\text{R,total}} - m_{\text{R,6''}}. \quad (1)$$

There may be further uncertainties in the MAGAUTO $R$-band magnitudes, but we expect they affect our estimates of the galaxy evolution rate by less than our statistical uncertainties (Section 4.2 and Appendix A).

The AGES redshift survey covers most of the NDWFS field. Spectra were obtained for well defined samples of galaxies in all the NDWFS photometric bands as well as for samples of AGNs. Our present sample combines limits from the AGES $I$-band and IRAC redshift sampling strategies (Table 1). In the $I$ band, AGES targeted all galaxies with $I < 18.5$ mag, complementing the $I < 16$ mag part of the sample with redshifts from the Sloan Digital Sky Survey (SDSS; Adelman-McCarthy et al. 2007) survey, and then randomly selected 20% of galaxies with $18.5 < I < 20$ mag for redshifts. Based on the IRAC optical magnitude distributions (see Figure 1), AGES chose

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### Table 1
Sample Selection and Redshift Targeting Limits for IRAC Bands

| Band | $m_{\text{comp}}(I)$ (mag) | $m_{\text{lim}}(I)$ (mag) | $I_{\text{comp}}$ (mag) | $I_{\text{lim}}$ (mag) | Redshift Completeness | Survey Area (deg$^2$) | Number of Galaxies |
|------|---------------------------|---------------------------|-------------------------|------------------------|-----------------------|---------------------|-------------------|
| C1 (3.6 μm) | 15.2 | 15.7 | 18.5 | 20 | 0.92 | 7.44 | 4905 |
| C2 (4.5 μm) | 15.2 | 15.7 | 18.5 | 20 | 0.93 | 7.44 | 5847 |
| C3 (5.8 μm) | 14.7 | 15.2 | 18.5 | 20 | 0.93 | 7.44 | 4367 |
| C4 (8.0 μm) | 13.2 | 13.8 | 18.5 | 20 | 0.96 | 7.44 | 3802 |

Notes: $m_{\text{lim}}(I)$ and $I_{\text{lim}}$ are the flux limits of the sample selection. $m_{\text{comp}}(I)$ and $I_{\text{comp}}$ are the limits where 100% of galaxies brighter than these magnitudes are targeted for redshifts. 30% of galaxies with $m_{\text{comp}}(I) \leq \leq m_{\text{lim}}(I)$ and 20% of galaxies with $18.5 \leq I \leq 20$ mag are targeted for redshifts.
C1–C4 ([3.6]–[8.0]) magnitude limits of $m_{\text{lim}}([X]) = 15.7$, 15.7, 15.2, and 13.8 mag, respectively. AGES then attempted to obtain redshifts for all galaxies brighter than $m_{\text{comp}}([X]) = 15.2, 15.2, 14.7, \text{and } 13.2$ for [3.6]–[8.0], respectively, and a randomly selected 30% of the galaxies in the magnitude ranges of $m_{\text{comp}}([X]) < [X] < m_{\text{lim}}([X])$. Figure 1 illustrates the combined effect of the optical and mid-IR sampling. We have a sample weight of $f_z = 1$ for $I \leq 18.5$ mag or $[X] \leq m_{\text{comp}}([X])$ and $f_z = 0.3$ for $I > 18.5$ mag and $m_{\text{comp}}([X]) < [X] < m_{\text{lim}}([X])$. The redshift completenesses are 92%, 93%, 93%, and 96% for the 3.6 to 8.0 μm bands, with no significant variations in the completeness with magnitude. Figure 2 shows the measured redshift distributions. The distributions peak at $z \approx 0.2$ and extend to $z \approx 1$, although we limit our analysis to $z \leq 0.6$. We excluded 155 AGNs (see Section 2.1) from the analysis. The final samples consist of 4905, 5847, 4367, and 3802 galaxies developed by Assef et al. (2008) based on the same data.

The choice of the 6″ aperture represents a compromise between smaller apertures that are more sensitive to aperture corrections and larger apertures that are more sensitive to contamination by other sources. Because of the magnitude limits required for the spectroscopy, the galaxies all have photometry in at least four of these bands, and on average have measurements in nine bands. From the Assef et al. (2008) models, we fit all available data (0.2–10 μm) with the early, late, and irregular templates for each galaxy and defined an early-type galaxy to be one in which 80% or more of the total 0.2–10 μm luminosity is assigned to the early-type template of Assef et al. (2008). Otherwise, we defined it as a late-type galaxy. After obtaining the spectral model for each galaxy, we used the templates (Assef et al. 2008) to compute the K-corrections that are needed for determining rest-frame luminosities. These K-corrections are consistent with the analytical approximations in Huang et al. (2007), as we show in Figure 4. The large scatter of the K-corrections in the [5.8] band is due to the spectral differences between the early- and late-type galaxies, where the PAH features contribute significantly to the late-type galaxies but not to the early-type galaxies. Although the [8.0] band is dominated by the PAH emission in late-type galaxies, the

2.1. SED Modeling

We fit the $B_{\text{W}}, R, I, z, J, K_s, K$, [3.6], [4.5], [5.8], and [8.0] 6″ diameter aperture magnitudes for each galaxy with combinations of spectral templates for early, late, and irregular galaxies.

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Figure 1. [3.6] spectroscopic selection. The points show the distribution of galaxies with measured redshifts. The [3.6] sample is defined by all galaxies with [3.6] $\leq 15.7$ mag and $I \leq 20$ mag. However, we only sample 30% of galaxies in the range of 15.2 $\leq [3.6] \leq 15.7$ and 18.5 $\leq I \leq 20$. The [4.5], [5.8], and [8.0] samples have similar definitions but with different magnitude limits.

Figure 2. Redshift distributions of our sample galaxies in the IRAC [3.6] to [8.0] bands. The histograms are binned with $\Delta z = 0.05$, and are slightly offset (less than 0.01) in redshift for clarity.

(A color version of this figure is available in the online journal.)

Figure 3. Rest-frame color ($B_{\text{W}} - R$) vs. magnitude plot for the [3.6] and [8.0] bands. The contours enclose 20% (bold), 40%, 60% and 80% of the objects with solid lines for early type and dashed lines for late type. We defined an early-type galaxy to be one in which 80% or more of the 0.2–10 μm luminosity is assigned to the early-type template of Assef et al. (2008). Otherwise, we defined it as a late-type galaxy.

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http://mizar.as.arizona.edu/rcod/hsred/.
scatter in the $K$-corrections is not as large as that in the [5.8] band because relatively few early-type galaxies are detected in the [8.0] band. The spectral fitting process also enables us to identify 155 galaxies that have significant AGN flux contributions (reduced $\chi^2 > 50$ in the template fits), which are then excluded for determining the LFs. These galaxies generally show the flat mid-IR power laws characteristic of AGNs (Stern et al. 2005).

We test the robustness of the SED model in the [5.8] and [8.0] bands. While we cannot directly test our estimate of the rest-frame magnitudes, we can examine how well the models reproduce the observed frame magnitudes as we use less information. In particular, we can fit the photometric data by dropping one or both of the [5.8] or [8.0] data points and then compare the predicted and measured magnitudes. This is a somewhat unfair comparison, of course, because for the real sample we always possess the [5.8] and [8.0] magnitudes. We carried out the experiment for three cases. The first case is simply how well the SED models fit the [5.8] and [8.0] data using the fits to all the photometric data (“both 5.8 and 8.0”). In the second case we fit the SED using neither the [5.8] nor the [8.0] data (“no 5.8 or 8.0”). Finally, in the third case we drop only the band we are considering (“no 5.8” for the [5.8] comparison and “no 8.0” for the [8.0] comparison). Figure 5 shows contours of the magnitude difference between the model and measured magnitudes. Figure 6 shows histograms of the magnitude differences for galaxies above the magnitude limits as compared to the distribution we would expect given the uncertainties in the magnitudes.

Based on these two plots, we can see that the $K$-corrections for the [5.8] channel are very robust. Even if we use neither the [5.8] nor the [8.0] magnitudes, the distributions of the magnitude differences is modest compared to our luminosity function.
bin widths and are largely consistent with the measurement uncertainties. This holds at 8 μm when we use all the available data, but there is significant scatter if we do not use the 5.8 and/ or 8 μm data. Nonetheless, while it is broader than our magnitude bins, it would affect our results little. After all, we always have the 5.8 and 8.0 μm data, and so we are generally closer to the “both 5.8 and 8.0” case than to the others. The redshifts of the 8.0 μm samples remain low enough that the 8.0 μm band generally samples portions of the PAH emission and so should remain well behaved. The worst-case scenario is that at z ~ 0.4 we are approaching the “no 8.0 μm” case for the 8.0 μm K-corrections.

3. LUMINOSITY FUNCTION DETERMINING METHODS

We used both the parametric maximum-likelihood method (STY; Sandage et al. 1979) and the nonparametric stepwise maximum-likelihood method (SWML; Efstathiou et al. 1988) to fit the luminosity functions. In the STY method, we parameterized the LF as a Schechter function

$$\Phi(M)dM = (0.4\ln 10)\phi_*(10^{0.4(M_*-M)})^{1+\alpha} \times \exp(-10^{0.4(M_*-M)})dM$$

and we allowed $M_*$ to evolve as

$$M_*(z) = M_*(0) - Qz$$

when fitting the LF, following the parameterization of Lin et al. (1999). We did not allow the normalization $\phi_*$ or the slope $\alpha$ of the LF to evolve since our sample size is not large enough to constrain the evolution of these parameters. Estimates of $\phi_*$ will also suffer from cosmic variance at low redshifts where we have little volume. In the SWML method, the LF is defined in bins $M_*-\Delta M/2 \leq M \leq M_*+\Delta M/2$ with value $\Phi_k$. In both methods, the parameters of the LFs in the STY method ($M_*, \alpha$, and $Q$) and the SWML ($\Phi_k$) method are calculated by maximizing the likelihood functions. Since the absolute normalization factor $\phi_*$ is not modeled in the likelihood function, the shape of the LF determined from the STY and SWML methods is not sensitive to the effects of large-scale structure. We calculated the normalization $\phi_*$ using the minimum variance method (Davis & Huchra 1982). Since the STY and minimum variance methods are widely used in determinations of LFs, we leave the details of the calculations to other references (e.g., Lin et al. 1996, 1999). We checked the STY and SWML calculations using both synthetic catalogs and by calculating the LFs using the 1/$\sqrt{V_{max}}$ method (Schmidt 1968; Avni & Bahcall 1980). The LFs from the 1/$\sqrt{V_{max}}$ method are in very good agreement with those determined from the SWML method, except for the very low luminosity bins where the 1/$\sqrt{V_{max}}$ results show a deficit of galaxies compared to the SWML method, probably due to the effects of large-scale structure. We only present the STY/ SWML results.

Each galaxy was assigned a weight based on the sampling strategy and the redshift completeness. The mean redshift completeness, $f_z = 0.92, 0.93, 0.93$, and 0.96 for the [3.6]–[8.0] bands, depends little on magnitude, and the sampling fraction $f_z = 1$ or 0.3 depends on the target magnitudes and the band (see Section 2.2, Table 1, and Figure 1). Thus, each galaxy has an overall statistical weight of $(f_z/f_z)^{-1}$. We included both the IRAC and I-band selection limits in our LF measurements. We also carried out the calculations using only the IRAC selection limits, and the resulting LFs are consistent with the full analysis. This is expected, since at the IRAC magnitude limits we are losing few galaxies due to the optical flux limit (see Figure 1).

We measured the LFs using the STY and SWML methods in three different ways for the [3.6]–[8.0] bands. First, we determined the LFs by applying the STY method to the entire redshift range ($z < 0.6$). This is essentially a pure luminosity evolution model since we did not allow the normalization $\phi_*$ or the slope $\alpha$ of the LF to evolve. Second, we applied the STY method to the three redshift bins $z < 0.2, 0.2 < z < 0.35$, and $0.35 < z < 0.6$. We chose the redshift bins as a balance between the number of galaxies (statistical uncertainties) and the bin width (averaging over cosmic time). We fixed the slope $\alpha$ and evolution parameter $Q$ to the values obtained from the first method and fitted only the normalization $\phi_*$ and $M_*$ in each redshift bin. This allows us to check whether the LFs evolve beyond the pure luminosity evolution model. Third, we measured the binned LFs with the SWML method in the three redshift bins and then fitted them jointly with Schechter functions, where we fixed the faint-end slope $\alpha$ to be the same in all bins but allowed the $M_*$ and the normalization $\phi_*$ to differ.

4. LUMINOSITY FUNCTIONS

Figures 7 and 8 show the resulting luminosity functions for the four bands. For each band we show the early-type, late-type, and total LFs for redshift bins of $0 < z < 0.2, 0.2 < z < 0.35$, and $0.35 < z < 0.6$. We show only the nonparametric SWML LFs and the result for the global parametric STY fit evaluated at the median of the redshift bin. Table 2 presents the parameters for the global STY fits with an evolving $M_*$, Table 3 presents the Schechter function fits to the SWML fits for the three redshift bins, and Table 4 presents the tabulated SWML LFs. The STY and SWML estimates of the luminosity functions are broadly consistent with each other, although we do find systematic mismatches in some cases (such as the faint-end slope of the total
Figure 7. Luminosity functions in the [3.6] and [4.5] bands for total, early-, and late-type galaxies. The LFs are plotted in three redshift bins with different colors. The lines are the LFs determined from the STY method fitting to the whole sample but plotted in different redshift bins. The discrete points are the LFs from the SWML method. The LFs from the STY and SWML methods are generally consistent with each other indicating our pure luminosity evolution parameterization in the STY method is reasonable.

(A color version of this figure is available in the online journal.)

LF in the [5.8] band with 1–2σ offsets). Given the flux limits of our survey, we can only determine the full LF parameters in the global fits and the lowest redshift bin. For the higher redshift bins we only sample the higher luminosity galaxies and cannot reliably determine the faint-end slope $\alpha$. The SWML LFs are well fitted by the Schechter functions with $\chi^2$/dof $< 1$ in all cases (Table 3), which also suggest that the SWML method slightly overestimates the error bars on the binned LFs.

We can compare our results to several recent mid-IR luminosity function measurements based on Spitzer data. Arnouts et al. (2007) and Babbedge et al. (2006) derived mid-IR luminosity functions based on the Spitzer Wide-Area Infrared Survey (SWIRE). Babbedge et al. (2006) used the 6.5 deg$^2$ ELAIS-N1 field of the SWIRE survey based on photometric redshifts and using the $V/V_{\text{max}}$ method to derive the luminosity functions based on approximately 34,000, 34,000, 14,000, and 17,000 galaxies to magnitude limits of 17.4 (30 μJy), 16.9 (30 μJy), 15.9 (50 μJy), and 15.3 (50 μJy) for the [3.6]–[8.0] bands, respectively. Arnouts et al. (2007) used the SWIRE data for the 0.85 deg$^2$ VVDS–0226–04 field using a combination of spectroscopic and photometric redshifts with limiting [3.6] magnitudes of 17.7 and 18.2, respectively. They derived a rest-frame $K$-band luminosity function using the $V/V_{\text{max}}$ and STY methods. The number of galaxies used in each analysis is unclear, but 1500 redshifts were available for the field. Huang et al. (2007) analyzed a subsample at [8.0] of the present data to 13.5 mag at $z < 0.3$ to estimate the local [8.0] luminosity function. We will convert from $K$ band back to the [3.6] band using the median rest-frame color of $K - [3.6] = 0.41$ mag found for the $z < 0.35$ AGES galaxies.
Figure 8. Luminosity functions in the [5.8] and [8.0] bands with the same sets of symbols/lines as in Figure 7. The LFs from the STY and SWML methods are generally consistent with each other indicating pure luminosity evolution.

Figure 9 presents the comparisons both for these Spitzer samples and the Two Micron All Sky Survey (2MASS) K-band luminosity function of Kochanek et al. (2001) for the total LF. We only show the parametric fits to the comparison luminosity functions over the magnitude range for which the other survey had data, and converted their results to Vega magnitudes and our cosmological model as necessary. These are summarized in Table 5. At [3.6] and [4.5], our results agree well with the other luminosity functions. In particular, at [3.6] all three parameters for the $z < 0.2$ bin are consistent with the local 2MASS values, although a small magnitude shift may be present, indicative of the luminosity evolution or luminosity definition problems we discuss in Section 4.2 and Appendix A. Our faint-end slopes in [3.6] and [4.5] for the total LF, $\alpha = -1.12 \pm 0.16$ and $-1.01 \pm 0.13$, are consistent with that in 2MASS, $-1.09 \pm 0.06$ (Kochanek et al. 2001). Parameter comparisons with Arnouts et al. (2007) and Babbedge et al. (2006) are somewhat moot due to their larger uncertainties. At [5.8] and [8.0] we can only compare to Babbedge et al. (2006) and our own earlier result in Huang et al. (2007). Huang et al. (2007) used a different sample definition and analysis method but was based on the same photometric and redshift surveys, and it is not surprising that our results are in agreement, except for the faint-end tail (see Figure 9). We do not agree with the general structure of the [5.8] and [8.0] LFs found by Babbedge et al. (2006), who found a better fit using power laws at the bright end rather than having the exponential truncation of the Schechter function. We see some very weak evidence for such an extension at [5.8] but no evidence for a global, bright-end power law.

4.1. Comparison between Early- and Late-Type Galaxies

In the [3.6], [4.5], and [5.8] bands we find that the early-type galaxies have shallower faint-end slopes than the late-type galaxies, in agreement with Arnouts et al. (2007), who also separated the early- and late-type galaxies using SED
models. The situation reverses at [8.0] with the early type showing a steeper faint-end slope, with 1.4σ confidence, than the late type. In particular, in the [3.6] and [4.5] bands our faint-end slopes for late-type galaxies, $\alpha_t = -1.40 \pm 0.18$ and $-1.29 \pm 0.17$, are consistent with the value $\alpha_t = -1.3 \pm 0.2$ from Arnouts et al. (2007), while in early-type galaxies there is about 1σ difference between our estimate ($\alpha_e = -0.6 \pm 0.3$) and the Arnouts et al. estimate ($\alpha_e = -0.3 \pm 0.2$). Our slopes are steeper than what Kochanek et al. (2001) found for their morphologically typed samples, $\alpha_e = -0.92 \pm 0.10$ (1σ difference) and $\alpha_t = -0.87 \pm 0.09$ (2.6σ difference), but this could be due to the different type definitions. Certainly, our present criterion of defining type based on a fixed luminosity fraction from the early-type template will tend to make the faint-end slope less negative because low-luminosity early-type galaxies are on average optically bluer (e.g., Figure 6 of Brown et al. 2007) and will hence be shifted toward the type boundary. The early- and late-type galaxies do show a systematic difference in their $K - [3.6]$ colors, with values of 0.35 and 0.54 mag for the median rest-frame color of the early- and late-type galaxies respectively. The shift for the late-type galaxies is presumably due to a larger PAH contribution in [3.6] for late-type galaxies, and it helps to explain why the $M_e$ of early- and late-type galaxies at [3.6] are more similar than they are at the K band. In addition, the differences between the faint-end slopes in this paper and Kochanek et al. (2001) also affect the estimates of $M_e$. The absence of strong PAH emission in the early-type galaxies leads to dramatic differences in the $\alpha_e$ between our estimate ($\sigma = 1.60 \pm 0.07$ versus $-1.85 \pm 0.13$).

### 4.2. Luminosity Evolution

Figure 10 shows the evolution of $M_e$ with redshift. We have three estimates of the evolution. One from the values of $Q$ derived in the global STY fits, one from the STY fits to the individual bins, and one from the Schechter function fits to the SWML luminosity functions. The differences between the three estimates are generally smaller than the statistical uncertainties, suggesting that our global STY fits are using an acceptable parameterization of the evolution. Where there are differences between the results, they are generally due to shifts in the faint-end slope $\alpha$ between the various fits. For example, the differences in the [5.8] bands are due to the SWML fits giving a shallower slope than the STY fits ($\alpha = -1.60 \pm 0.07$ versus $-1.85 \pm 0.13$).
If we transform the Kochanek et al. (2001) K-band points to [3.6], they lie on the redshift zero extrapolation of our [3.6] results, and if we transform the Arnouts et al. (2007) results back to [3.6] they also lie on our trend. The $M_\ast$ values from Babbedge et al. (2006) are also consistent with our trend for the [3.6] and [4.5]. Since $M_\ast$ is correlated with the faint-end slope, we corrected for the correlation in this comparison by using the $M_\ast$–$\alpha$ confidence contours from our measurements to shift the other results for $M_\ast$ to match our estimates of $\alpha$. Because of the very different power-law form used by Babbedge et al. (2006) at [5.8] and [8.0] we cannot compare to their results in the longer wavelength bands.

At [3.6] and [4.5] the evolution rates depend little on galaxy type, both in our results and in the earlier studies. The behavior is very different at [5.8]. At [5.8] we see essentially no evolution for the late-type galaxies and a steady brightening of the early-type galaxies. The enormous uncertainty in early-type galaxies at [8.0] does not allow us to perform a meaningful comparison.

The [8.0] band should trace the star formation rate through the emission from the PAH features. Our LF evolution rate $Q = 1.8 \pm 1.1$ in [8.0], equivalent to $\beta = 2.4 \pm 1.5$ for $L_{\text{FIR}} \propto (1 + z)^\beta$, is consistent with other estimates for the evolution of star formation (e.g., $\beta = 2.7 \pm 0.6$, Hopkins 2004; $\beta = 3.8 \pm 0.5$, Villar et al. 2008). The [3.6] and [4.5] bands largely trace the Rayleigh–Jeans tail of the stellar emission, where the LFs are expected to evolve passively. The passive evolution model is a specific pure luminosity evolution model, where the evolution rate $Q$ should follow that from an aging stellar population. Arnouts et al. (2007) estimated that the passive evolution for the K band was $Q \sim 0.7–1.0$ from early- to late-type galaxies. If we assume that the [3.6] and [4.5] bands have similar passive evolution rates, our late and total LF evolution rates ($Q \sim 0.9–1.2$) are consistent with the passive evolution model, while our early-type LF evolution rates ($Q \sim 1.3–1.4$) are $\sim 1.5\sigma$ faster than the predictions. If we include the data from Kochanek et al. (2001) and Arnouts et al. (2007), the $Q$ value for early-type galaxies at [3.6] is slightly slower with $Q = 1.20 \pm 0.16$. We note that the B-band evolution rate for early-type galaxies, $Q \sim 0.9$, from Brown et al. (2007) is also slower than our estimate.

Our greatest concern in these estimates is that redshift-dependent biases in the total magnitudes are mimicking evolution. In our original calculation, we simply used the total $M_{\text{AG\_AUTO}}$ magnitudes from the IRAC Shallow Survey and found still faster evolution rates with $\Delta Q = +0.3$. This drove our investigation of the difference in the aperture and $M_{\text{AG\_AUTO}}$ total magnitudes where we found a difference of about 0.15 mag over the range from $z = 0$ to 0.5 between the optical and mid-IR photometry. That led us to the present approximation (see Section 2). This needs to be investigated further, but a complete

| Band | Type | Mag | $dN/dM$ ($h^3\text{Mpc}^{-3}\text{mag}^{-1}$) |
|------|------|-----|----------------------------------------|
| [3.6] | All | −19.00 | 2.0E−1 (1.1E−1) |
| [3.6] | All | −19.25 | 9.6E−2 (6.5E−2) |
| [3.6] | All | −19.50 | 1.0E−1 (5.2E−2) |
| [3.6] | All | −19.75 | 2.0E−2 (2.1E−2) |
| [3.6] | All | −20.00 | 2.7E−2 (2.0E−2) |
| [3.6] | All | −20.25 | 3.9E−2 (2.3E−2) |
| [3.6] | All | −20.50 | 6.1E−2 (2.8E−2) |
| [3.6] | All | −20.75 | 3.4E−2 (1.8E−2) |
| [3.6] | All | −21.00 | 1.5E−2 (9.4E−3) |
| [3.6] | All | −21.25 | 1.5E−2 (7.6E−3) |
| [3.6] | All | −21.50 | 1.7E−2 (8.0E−3) |
| [3.6] | All | −21.75 | 1.5E−2 (7.1E−3) |
| [3.6] | All | −22.00 | 1.9E−2 (8.5E−3) |
| [3.6] | All | −22.25 | 1.1E−2 (5.1E−3) |
| [3.6] | All | −22.50 | 1.1E−2 (5.0E−3) |
| [3.6] | All | −22.75 | 1.1E−2 (5.1E−3) |
| [3.6] | All | −23.00 | 9.3E−3 (4.1E−3) |
| [3.6] | All | −23.25 | 9.2E−3 (4.0E−3) |
| [3.6] | All | −23.50 | 7.1E−3 (3.2E−3) |
| [3.6] | All | −23.75 | 6.3E−3 (2.8E−3) |
| [3.6] | All | −24.00 | 5.0E−3 (2.2E−3) |
| [3.6] | All | −24.25 | 4.0E−3 (1.8E−3) |
| [3.6] | All | −24.50 | 2.8E−3 (1.3E−3) |
| [3.6] | All | −24.75 | 2.2E−3 (1.0E−3) |
| [3.6] | All | −25.00 | 1.1E−3 (5.6E−4) |
| [3.6] | All | −25.25 | 9.3E−4 (5.0E−4) |
| [3.6] | All | −25.50 | 3.0E−4 (2.3E−4) |
| [3.6] | All | −25.75 | 2.1E−4 (6.0E−5) |
| [3.6] | All | −26.00 | 5.1E−5 (3.0E−5) |
| [3.6] | All | −26.25 | 9.8E−6 (1.4E−5) |
| [3.6] | All | −26.50 | 3.0E−5 (1.2E−5) |
| [3.6] | All | −26.75 | 6.0E−6 (5.0E−6) |

(This table is available in its entirety in a machine-readable form in the online journal. A portion is shown here for guidance regarding its form and content.)
There is generally good agreement between our LFs and other measurements, except in the [5.8] and [8.0] bands where Babbedge et al. (2006) found that the LFs were better fitted by power laws.

(A color version of this figure is available in the online journal.)

### Table 5

Comparison with Other IR LFs

| Sample                  | Band     | Type         | Redshift | $\alpha$        | $M_\star - 5 \log h$ (mag) | $\phi_\star$ $(10^{-2} h^3 \text{Mpc}^{-3})$ |
|------------------------|----------|--------------|----------|-----------------|-----------------------------|-----------------------------------------------|
| Kochanek et al. (2001) | Converted to [3.6] | All | 0.02 | $-1.09 \pm 0.06$ | $-23.85 \pm 0.05$ | $1.16 \pm 0.10$ |
|                        |          | Early        |          | $-0.92 \pm 0.10$ | $-23.88 \pm 0.10$ | $0.45 \pm 0.06$ |
|                        |          | Late         |          | $-0.87 \pm 0.09$ | $-23.52 \pm 0.09$ | $1.01 \pm 0.13$ |
| Arnouts et al. (2007)  | Converted to [3.6] | All | 0.3 | $-1.1 \pm 0.2$ | $-24.3 \pm 0.6$ | $1.3 \pm 0.6$ |
|                        |          | 0.5          |          | $-1.1 \pm 0.2$ | $-24.4 \pm 0.3$ | $1.0 \pm 0.4$ |
|                        |          | 0.7          |          | $-1.12 \pm 0.06$ | $-24.5 \pm 0.1$ | $1.0 \pm 0.1$ |
|                        |          | Early        |          | $-0.3 \pm 0.2$ | $-23.8 \pm 0.3$ | $0.68 \pm 0.09$ |
|                        |          | 0.5          |          | $-0.3 \pm 0.2$ | $-23.9 \pm 0.2$ | $0.43 \pm 0.05$ |
|                        |          | 0.7          |          | $-0.29 \pm 0.12$ | $-24.1 \pm 0.1$ | $0.38 \pm 0.03$ |
|                        |          | Late         |          | $-1.3 \pm 0.2$ | $-24.5 \pm 0.3$ | $0.6 \pm 0.3$ |
| Babbedge et al. (2006) |          | All          | 0.00–0.25 | $-0.9$ | $-23.9 \pm 0.1$ | 1.0 |
|                        |          |              | 0.25–0.50 | $-1.0$ | $-24.3 \pm 0.1$ | 1.3 |
|                        |          |              | 0.50–1.00 | $-0.9$ | $-24.1 \pm 0.1$ | 2.0 |
|                        |          |              | 0.00–0.25 | $-0.9$ | $-23.9 \pm 0.1$ | 1.3 |
|                        |          |              | 0.25–0.50 | $-1.0$ | $-24.1 \pm 0.1$ | 2.0 |
|                        |          |              | 0.50–1.00 | $-1.1$ | $-24.1 \pm 0.1$ | 2.2 |
| Huang et al. (2007)    |          | All          | 0.0–0.3  | $-1.38 \pm 0.04$ | $-27.69 \pm 0.08$ | 0.32 |
|                        |          | PAH          |          | $-1.26 \pm 0.04$ | $-27.57 \pm 0.08$ | 0.35 |
| This Paper             |          | All          | 0.24     | $-1.12 \pm 0.16$ | $-24.29 \pm 0.18$ | 1.08 \pm 0.03 |
|                        |          |              | 0.25     | $-1.02 \pm 0.13$ | $-24.20 \pm 0.16$ | 1.07 \pm 0.03 |
|                        |          |              | 0.24     | $-1.85 \pm 0.13$ | $-26.03 \pm 0.17$ | 0.27 \pm 0.01 |
|                        |          |              | 0.20     | $-1.42 \pm 0.12$ | $-27.84 \pm 0.26$ | 0.48 \pm 0.01 |
re-analysis of the survey photometry is well beyond the scope of our analysis. However, our investigations in Appendix A suggest that the redshift-dependent magnitude definition problem in our current scheme is less severe, with systematic uncertainties of \( \Delta Q < 0.1 \).

4.3. Density Evolution

Figure 11 shows the evolution of \( \phi_* \) for the same three methods discussed in Section 3. In the global STY fit, \( \phi_* \) is a constant. In the STY fit to the individual redshift bins combined with a Schechter function fit to the SWML LF, the \( \phi_* \) are allowed to differ between the redshift bins. We estimated the cosmic variance in our sample using the estimator

\[
\sigma_Y^2 = \frac{1}{V^2} \int \xi(|r_1 - r_2|) dV_1 dV_2
\]

(e.g., Peebles 1980; Somerville et al. 2004). We adopted a power-law correlation function \( \xi = (r / r_0)^{-\gamma} \) with \( r_0 = 5.6, 5.7, \) and 3.6 \( h^{-1} \)Mpc and \( \gamma = 1.8, 2.1, \) and 1.7, for total, early-, and late-type galaxies, respectively, measured from the SDSS survey (Zehavi et al. 2005). In our three redshift bins of \( z < 0.2, \) 0.2 \( < z < 0.35, \) 0.35 \( < z < 0.6, \) and the total range \( z < 0.6, \) we obtained cosmic variance estimates of 20\%, 15\%, 10\%, and 8\% for the total population, 18\%, 13\%, 8\%, and 7\% for the early-type, and 15\%, 11\%, 8\%, and 6\% for the late-type galaxies. The cosmic variances we obtained are comparable to the statistical uncertainties in \( \phi_* \) for the SWML LFs.

In general, we see no convincing evidence for density evolution, with the exception of the early-type galaxies in the [3.6] and [4.5] bands, where we seem to see a steady decline. For the STY method (fixed \( \phi_* \)) we obtained \( \phi_* = 0.44 \pm 0.05 \) and \( 0.37 \pm 0.04 \) \( (10^{-2} \ h^3 \)Mpc\(^{-3}) \) for early-type galaxies in [3.6] and [4.5] for the full redshift range of \( z \leq 0.6 \). Including the uncertainties from cosmic variance, the \( \phi_* \) values from SWML for early-type galaxies are higher than the STY values by 1.3\% and 1.6\% in the first redshift bin \( z < 0.2 \) for [3.6] and [4.5], and lower than the STY value by 2.0\% in the third bin \( 0.35 < z < 0.6 \) for [3.6]. For the second bin \( 0.2 < z < 0.35 \), the two methods yielded consistent results. However, this trend does not extend to \( z = 0 \), when we compare to the \( \phi_* \) found in the local 2MASS sample (Kochanek et al. 2001), and it suggests that the low-redshift point from AGES is high due to cosmic variance rather than due to rapid evolution. We note that the early-type galaxies in Kochanek et al. (2001) are morphologically selected, which might also cause the difference. The early-type sample in Arnouts et al. (2007) is also based on the SED fitting, and there is a modest decline of \( \phi_* \) with redshift in their three bins as well, consistent with our trend, but the absolute values of \( \phi_* \) do not match between the two samples. For the remaining cases there is no evidence for any significant density evolution.

Figure 10. Evolution of \( M_* \) in the IRAC channels for the total (black, square, dot-dashed), early- (red, circle, dotted) and late- (blue, triangle, dashed) type galaxies. The lines are the results from the STY fit to the full sample. The triangles, circles, and squares are our AGES results, where the filled symbols are the results from fitting Schechter functions to the binned SWML LFs, and the open symbols are the results from the STY fits to the individual redshift bins. We do not plot the error bars from the STY fits in the individual redshift bins for clarity, but they are similar to those determined from the SWML LFs. The diamonds, stars, and "+" signs are results from Kochanek et al. (2001), Arnouts et al. (2007), and Babbedge et al. (2006) after correcting for color, cosmology, magnitude system, and faint-end slope differences. In the [3.6] and [4.5] bands, which trace the Rayleigh–Jeans tail of the stellar emission, the evolution of \( M_* \) is consistent with a passive evolution model, while in the [8.0] band, which is sensitive to star formation, the evolution of \( M_* \) is consistent with other estimates for the evolution of star formation rates.

(A color version of this figure is available in the online journal.)
We can also compare the measurements of density evolution with those in optical bands. While the late-type galaxies are generally found to have no significant density evolution within $z < 1$ consistent with our results, there are several studies suggesting a significant density evolution for early-type galaxies within $z < 1$ from 40% to 400% (Zucca et al. 2006; Faber et al. 2007; Bell et al. 2004). However, there is also evidence for little density evolution in early-type galaxies ($z < 0.6$; however, adding the data points from Arnouts et al. (2007) and Kochanek et al. (2001) and considering the cosmic variance, the combined data do not provide a definitive answer.

4.4. The Luminosity Density and its Evolution

Assuming that we can extrapolate the luminosity functions beyond the magnitude limits of the samples, we can compute the luminosity densities from the LFs as $\rho_{vL_v} = \phi_v (v L_{v,0}) \Gamma(2 + \alpha)$, where we obtain $L_{v,0}$ through our $M_v$ and IRAC zero points. The results will be insensitive to the value of the faint-end slope when $\alpha \sim -1$. However, when the faint-end slope is steep, the uncertainties introduced by $\alpha$ are large. In particular, for the case of the early-type galaxies at [8.0], the result is divergent because $\alpha \simeq -2.0$. Figure 12 shows the luminosity densities for our three standard methods, except for the early-type galaxies at [8.0] because of the large uncertainties. In general, we see a trend of increasing luminosity density with higher redshifts, with the weakest trends for the early-type galaxies at [3.6] and [4.5].

Even passive evolution models predict that the luminosity density increases with redshift. Since the evolution of $M_v$ and $\phi_v$ for late-type and total galaxies in [3.6] and [4.5] are consistent with the predictions from passive evolution (constant $\phi_v$ and $Q \sim 1$), the evolution in luminosity density must also be consistent with the predictions. For early-type galaxies, the evolution of luminosity density will tend to provide a more robust test for the passive evolution models than examinations of the individual Schechter parameters because they are less sensitive to the strong correlations between $\alpha$ and $M_v$. Combining the data from Kochanek et al. (2001) and Arnouts et al. (2007), the luminosity density evolution in [3.6] is at least flat. We compare this with the expected luminosity density evolution from the passive evolution model. In the passive evolution model, $\alpha$ and $\phi_v$ are constants, and hence the luminosity density scales with $L_\odot$. Using the $K$-band passive evolution rate of $Q = 0.7$ for early-type galaxies (Arnouts et al. 2007), $L_\odot$ should dim by 0.5 mag from $z = 0.7$ to 0. The constant trend of the [3.6] band luminosity density deviates from the passive evolution model and indicates an increase of stellar mass of 40 ± 20% from $z = 0.7$ to 0 assuming a constant mass-to-light ratio at $z = 0$. When we compare the first and last data points from Kochanek et al. (2001) and Arnouts et al. (2007). We fitted all the data with a power law and obtained $\log \frac{\rho_{vL_v}}{L_\odot h^{\text{Mpc}^{-3}}} = (7.18 \pm 0.04) - (0.20 \pm 0.07)z$. (5)

This indicates an increase of stellar mass of 87 ± 30% from $z = 0.7$ to 0 for early-type galaxies. If we remove the 2MASS point based on the morphological definition and use only the six remaining points based on a SED definition for early-type galaxies, the luminosity density evolution shows even larger

Figure 11. Evolution of $\phi_v$ in the IRAC channels. The symbols and lines styles are the same as in Figure 10. Babbedge et al. (2006) did not provide error bars for their estimates of $\phi_v$. The cosmic variances of approximately 20%, 15%, and 10% for the redshift bins of $z < 0.2$, $0.2 < z < 0.35$, and $0.35 < z < 0.6$ are not included in the uncertainties.

(A color version of this figure is available in the online journal.)
differences from a passive evolution model. Our results are consistent with the flat $B$-band luminosity density evolution for early-type galaxies (Bell et al. 2004; Faber et al. 2007; Brown et al. 2007), and the $K$-band analysis of Arnouts et al. (2007) who find the stellar mass for early-type galaxies has increased by 100% from $z = 1.2$ to 0.

In Figure 13, we shift the luminosity densities to $z = 0.1$ and combine them with earlier results scaled to that redshift at shorter wavelengths from the near-IR through the UV, based on results from GALEX, SDSS, and 2MASS (Arnouts et al. 2005, Bell et al. 2003, Jones et al. 2006). The “spectrum” given by the luminosity density is typical of a moderately star-forming galaxy, as we illustrate by fitting the implied SED with the template models from Assef et al. (2008). The luminosity density spectrum has an early-type fraction of $e = 0.25$.

4.5. Comparison with a Semianalytical Model

We can also compare our LFs with the predictions from the recent semianalytical models of Lacey et al. (2008). Lacey et al. (2008) combined a semianalytical hierarchical galaxy formation model based on cold dark matter, a theoretical stellar population synthesis model for stellar emission, and a theoretical radiative transfer model for dust absorption and emission. They also assumed a top-heavy initial mass function (IMF) in starbursts and a normal solar neighborhood IMF for quiescent star formation. The model was tuned to reproduce the $B$, $K$, and 60 $\mu$m LFs, and several observed interrelationships between galaxy luminosity, gas mass, metallicity, size, and the fraction of spheroidal galaxies.

Figure 14 shows the comparison between our SWML LFs at $z < 0.2$, $0.2 < z < 0.35$, and $0.35 < z < 0.6$ to the theoretical models at $z = 0.1$, $z = 0.25$, and $z = 0.5$. Note that there are small mismatches between our median redshifts of $z = 0.15$, 0.25, and 0.45 and those of the models. In general, the models match our observed [3.6] and [4.5] LFs well, they are roughly
consistent at [8.0], and they fail to reproduce the [5.8] LFs. At [3.6] and [4.5], the shape of model LFs is consistent with the Schechter form at \( \lesssim M - 22 \) mag, and steepen at the faint end consistent with the tail of our SWML LFs. The model slightly overpredicts the [8.0] LFs at the bright end, and underpredicts the faint-end LFs. The significantly worse match at [5.8] is likely due to problems with the PAH features in the theoretical models. This affects the [5.8] more than the other bands because at [5.8] the sample is composed of a mixture of stellar and ISM emission and has the largest scatter in its \( K \)-corrections (see Figure 4).

We can also compare the LF evolution between the models and our measurements. At [3.6] and [4.5], the model predicts little LF evolution at the bright end, although the match of the evolution rates at [8.0] is better. Lacey et al. (2008) also modeled the early- and late-type LFs separately, where the late-type galaxy LFs are similar to the total LFs except for the normalization, and the early-type LFs have significant flatter faint-end slopes. This is also consistent with our measurements.

5. DISCUSSION

The spectroscopy from the AGES survey has allowed us to measure the mid-IR (3.6, 4.5, 5.6, and 8.0 \( \mu \text{m} \)) luminosity functions for \( z < 0.6 \) with greater precision than existing mid-IR surveys which have largely relied on photometric redshifts. The bluest bands agree well with local \( K \)-band luminosity functions, possibly with some effects from the PAH feature in the 3.6 \( \mu \text{m} \) band: the early- and late-type galaxies have similar characteristic magnitudes and the early-type galaxies have shallower faint-end slopes. As we move to the redder bands, the early-type galaxies exhibit fainter break magnitudes and steeper faint-end slopes relative to the late-type galaxies. In general our results agree well with other recent mid-IR studies based largely on photometric redshifts by Franceschini et al. (2006), Babbedge et al. (2006), and Arnouts et al. (2007). Although we have better statistics and use only spectroscopic redshifts, our study is limited to lower redshifts. The one major exception is that we find that Schechter function fits work reasonably well at 5.8 and 8.0 \( \mu \text{m} \), as Huang et al. (2007) also found for 8.0 \( \mu \text{m} \) based on a subsample of galaxies with \( z < 0.3 \) in our field. This is in disagreement with the power-law fits adapted by Babbedge et al. (2006) for these bands.

Photometric redshifts are known to work well for the typical galaxy (e.g., Section 3.1, Babbedge et al. 2006) which is why our luminosity functions broadly agree with those based solely or largely on them. Where spectroscopic redshifts have an edge is on the wings of the luminosity function, where magnitude limited samples have few objects because the high-luminosity objects are rare and the volume in which low-luminosity objects can be found is small. These parts of the luminosity function, well away from \( L_* \), are quickly altered given even a small number of catastrophic photo-\( z \) redshift errors for the far more numerous \( L_* \) galaxies. The general tendency will be to weaken the exponential cutoff of a Schechter function at high luminosity and to steepen the slope at low luminosity. While we have no direct evidence that this is the explanation, this is exactly the trend of our differences with the longer wavelength SWIRE luminosity functions (Babbedge et al. 2006).

We find no convincing evidence for density evolution in our sample, and a pure luminosity evolution model appears to work...
also extend measurements of the galaxy luminosity density at $z = 0.1$ into the mid-IR. The luminosity density spectrum is that of a mildly star-forming galaxy where the emission drops from the near-IR to a minimum near $5 \, \mu m$ and rises again due to PAH emission.

Our results at low redshift would be significantly improved by combining our sample with a complete redshift survey of the brighter mid-IR sources in the wider area SWIRE fields, to better constrain the low-redshift, high-luminosity sources, and with a fainter sample in a narrow field (e.g., the DEEP2 results for the Extended Groth Strip) to better constrain the faint end of the luminosity function and extend the results to higher redshifts. Within the Boötes field itself we can achieve many of the same goals using photometric redshifts. In particular, Assef et al. (2008) have developed a set of templates that extend through all four IRAC bands, which would probably give better results than most existing studies which have truncated their templates near the $4.5 \, \mu m$ band due to a lack of good templates for the longer wavelengths. Since our present analysis used the rest-frame $8 \, \mu m$ results from the Assef et al. (2008) templates, which are based on data that extend only to $5 \, \mu m$ for sources at $z = 0.6$, it would also be useful to extend the templates through the MIPS $24 \, \mu m$ band.

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APPENDIX
STANDARDIZING THE IRAC PHOTOMETRY

As we attempted to measure the evolution of the LFs with redshift, it became clear that evolving magnitude definitions could be a serious problem since a 0.1 mag drift in the magnitude definition from $z = 0$ to 0.5 corresponds to a $\Delta Q \approx 0.2$ change in the evolution rate. The existence of some problems was easily diagnosed by redshift dependent changes in Kron radii between bands, and the behavior of aperture versus Kron magnitudes. The cleanest test for evolution is to synthesize metric aperture magnitudes subtending a fixed physical scale, as these should have no redshift dependence if there is no evolution. We use this method to test whether there are additional corrections needed beyond those discussed in Section 2. Unfortunately, finite metric apertures sample different fractions of galaxies depending on their luminosity (size), so we must model the luminosity dependence while searching for a redshift dependence. Figure 15 shows the difference, $m_{18} - m_{Kron}$, between the $18 \, h^{-1}$ kpc diameter metric magnitude ($m_{18}$) and Kron magnitude for the $3.6 \, \mu m$ band both for the data

reasonably well. The $M_*$ for the total galaxy population evolves as $Q_\nu$ with $Q_\nu \approx 1.1$--1.2 in the $[3.6]$ and $[4.5]$ bands, which probe the stellar mass, and the evolution rates are consistent with the $K$-band passive evolution models of Arnouts et al. (2007, $Q_\nu \approx 1.0$). We measured the evolution rate $Q_\nu \approx 1.8$ in the $[8.0]$ band, which is sensitive to star formation and consistent with other estimates for the evolution of star formation (Hopkins 2004; Villar et al. 2008). The rate of evolution agrees well with the scalings from 2MASS, Arnouts et al. (2007) and Babbedge et al. (2006) at $3.6 \mu m$. At $[3.6]$ and $[4.5]$, the evolution of $M_*$ and $\phi_*$ for early-type galaxies suggests possible deviations from passive evolution models, however, with large uncertainties. The evolution of luminosity density for early-type galaxies provides a more robust test for deviations from the passive evolution model and suggests that the stellar mass for early-type galaxies has increased by $87 \pm 30\%$ from $z = 0.7$ to $z = 0$. We also compared our LFs with the recent semianalytical model from Lacey et al. (2008). While the match between the model and observations is excellent at $[3.6]$ and $[4.5]$, it is worse at $[8.0]$, and at $[5.8]$ the model failed to reproduce the $[5.8]$ LFs.
and the mean difference found assuming de Vaucouleurs profile galaxies with \( L \propto R^{1.6} \) (Bernardi et al. 2003). We see that the dominant trend comes from the luminosity. To estimate the redshift biases, we fit

\[
 m_{18} - m_{\text{Kron}} = \begin{cases} 
 a(M_{\text{Kron}} - M_0)^2 + b z + c & : M_{\text{Kron}} < M_0 \\
 b z + c & : M_{\text{Kron}} \geq M_0 \end{cases}
\]

(A1)

using a one-sided quadratic term for the luminosity trend and adding a linear (false) evolution with redshift. The parameters are the mean offset \( c \), the amplitude of the quadratic dependence on luminosity \( a \), the luminosity \( M_0 \) above which the metric aperture underestimate the flux, and the redshift bias \( b \). As we show in Figure 15, the one-sided quadratic term models the mean luminosity trend well. The resulting estimates for the redshift biases are \( b = -0.02 \pm 0.02 \) and \( 0.08 \pm 0.02 \) for the 3.6 and 4.5 \( \mu \)m bands. These are significantly smaller than the statistical uncertainties (\( \Delta Q \sim 0.5 \)) in the evolution rates, so we decided to apply no further corrections. In the 5.8 and 8.0 \( \mu \)m bands, our simple model failed to reproduce the measured difference between \( m_{18} \) and \( m_{\text{Kron}} \) possibly due to the complexity that the PAH emission from star formation may not follow the de Vaucouleurs profile. Since our tests in the 3.6 and 4.5 \( \mu \)m bands show no significant redshift-dependent biases, we adopted a consistent photometry scheme in the 5.8 and 8.0 \( \mu \)m bands the same as that for the 3.6 and 4.5 \( \mu \)m bands.

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