Potassium Current and the Effect of Cesium on this Current during Anomalous Rectification of the Egg Cell Membrane of a Starfish

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ABSTRACT The kinetics of the membrane current during the anomalous or inward-going rectification of the K current in the egg cell membrane of the starfish *Mediaster aequalis* were analyzed by voltage clamp. The rectification has instantaneous and time-dependent components. The time-dependent increase in the K conductance for the negative voltage pulse as well as the decrease in the conductance for the positive pulse follows first-order kinetics. The steady-state conductance increases as the membrane potential becomes more negative and reaches the saturation value at about -40 mV more negative than the K equilibrium potential, $V_K$. The entire K conductance can be expressed by $g_K = g_K' \cdot n$; $g_K'$ represents the component for the time-independent conductance which depends on $V-V_K$ and $[K^+]_o$, and $n$ is a dimensionless number (1 -> n -> 0) and determined by two rate constants which depend only on $V-V_K$. Cs$^+$ does not carry any significant current through the K channel but blocks the channel at low concentration in the external medium. The blocking effect increases as the membrane potential is made more negative and the potential-dependent blocking by the external Cs$^+$ also has instantaneous and time-dependent components.

Katz (1949) studied the membrane property of the frog skeletal muscle fiber in isotonic potassium sulfate solution, and found that the membrane resistance was low for the inward current but was high for outward current. This property has been referred to as the inward-going or anomalous rectification and others have studied this extensively (Hodgkin and Horowicz, 1959; Adrian and Freygang, 1962 a, b; Nakajima et al., 1962; Adrian, 1964, 1969; Horowicz et al., 1968; Nakamura et al., 1965; Adrian et al., 1970; Almers, 1971, 1972). Recently, a similar rectification has been found in the membrane of an egg cell of a tunicate (Takahashi et al., 1971; Miyazaki et al., 1974) and of a starfish (Hagiwara and Takahashi, 1974; Miyazaki et al., 1975 b). In both cases the membrane current for the rectification is carried by K ions under normal conditions. The present study deals with the inward-going or anomalous rectification in the membrane of a giant egg cell (about 1 mm in diameter) of the starfish *Mediaster aequalis*. The
kinetics of the $K$ current during the rectification and blocking effect of Cs upon the $K$ channel were analyzed by voltage clamp technique.

**MATERIALS AND METHODS**

Immature egg cells of the starfish *Mediaster aequalis* were used. The collection of the eggs and the experimental technique were similar to those described previously (Hagiwara et al., 1975). The experiments were performed at room temperature (21–22°C). The compositions of the major solutions used are listed in Table I. Most of the experiments were performed in Na-free Tris media (solutions A–D). The replacement of NaCl with Tris-Cl altered neither the resting potential nor the membrane current for the ranges of the $K$ concentration and the membrane potential examined in the present work. The membrane of a starfish egg cell shows an action potential when it is depolarized (Miyazaki et al., 1975; Hagiwara et al., 1975). Corresponding to this, a transient inward current appears when the membrane potential is clamped with a positive-going voltage pulse. The inward current depends on the external Ca ++ and Na +, and is abolished by replacing Ca ++ with Mn ++ even when the normal amount of Na + is present. The transient inward current disturbed the measurement of the instantaneous membrane conductance with a

| TABLE I |
|--------------------------|
| **COMPOSITIONS OF SOLUTIONS** |
|                          | KCl  | NaCl  | CaCl₂ | MnCl₂ | MgCl₂ | Tris OH | HCl |
|--------------------------|------|-------|-------|-------|-------|---------|-----|
| Normal saline            | 10 mM| 470 mM| 10 mM | 50 mM | 10 mM | 6.7 mM  |     |
| Solution A               | 10 mM|       | 10 mM | 50 mM | 574 mM|         | 383 |
| Solution B               | 25 mM|       | 10 mM | 50 mM | 556 mM|         | 371 |
| Solution C               | 50 mM|       |       | 50 mM | 526 mM|         | 351 |
| Solution D               | 100 mM|     | 10 mM | 50 mM | 466 mM|         | 311 |
| Solution E               | 25 mM| 455 mM|       | 10 mM | 50 mM |         | 6.7 |

pH was adjusted to 7.7 by Tris OH-HCl.
Tris OH: Tris (hydroxymethyl)aminomethane.

positive-going voltage pulse. Therefore, some of the experiments were performed in solution E which contains MnCl₂ instead of CaCl₂. The solution contained NaCl instead of Tris-Cl to avoid possible complex salt formation of Mn with Tris. CsCl was simply added to each solution. Since the concentration of CsCl never exceeded 5 mM it did not alter the tonicity significantly.

Microelectrodes filled with 3 M KCl were used in all experiments. The technique of voltage clamp is similar to that described previously (Hagiwara et al., 1975). The rise time constant of the voltage step was about 2 ms. The membrane current and potential were acquired and analyzed by a PDP 8E computer (Digital Equipment Corporation, Maynard, Mass., time resolution 0.125 ms) and recorded with an X-Y plotter. The holding membrane potential for the voltage clamp was always the resting or zero-current membrane potential.

**RESULTS**

**Instantaneous $K$ Currents**

The average resting or zero-current membrane potential $V_o$ of the egg cell in the normal saline containing 10 mM K was $-73 \pm 3$ mV (SD, $n = 10$). This was not
altered by replacing the NaCl in the solution with Tris-Cl (solution A). The resting membrane behaved as a nearly perfect K electrode for K concentrations above 10 mM, and this is true in both the Na and the Tris solutions. The Cl permeability is negligible since the membrane potential shows no significant change for the replacement of the external Cl with an impermeant anion such as methanesulfonate. The results agree with those obtained with egg cells from other species of starfish (Hagiwara and Takahashi, 1974; Miyazaki et al., 1975 b).

![Figure 1](image)

**Figure 1.** Traces of membrane currents under voltage clamp condition at four different K concentrations (10, 25, 50, and 100 mM) in Na-free media. Holding membrane potential, at resting potential: -71 mV in 10 mM K, -48 mV in 25 mM K, -33 mV in 50 mM K, and -17 mV in 100 mM K. The figure in each trace indicates the magnitude of the potential step (ΔV) applied from the holding potential. Diameter of the cell, 900 μm.

The membrane currents during voltage clamp at various membrane potential levels and at four different K concentrations (10, 25, 50, and 100 mM) in Na-free solutions are shown in Fig. 1. For negative ΔV a step change in the membrane potential was associated with an instantaneous inward current, $I_o$ and the magnitude of the current then increased gradually to a maximum value. When ΔV was positive the outward current decreased gradually. Fig. 2 shows current-voltage relations for the instantaneous current, $I_o$ (continuous lines), and for the current at the steady state, $I_s$ (broken lines), obtained from the results shown by Fig. 1.
Both the steady-state data and the instantaneous data show inward-going rectification. The instantaneous conductance $g_\circ$ can be obtained by

$$I_\circ = g_\circ \cdot (V - V_0) = g_\circ \cdot \Delta V.$$  

(1)

The zero-current membrane potential $V_0$ behaves as a K electrode. Unlike the frog skeletal muscle fiber the Cl permeability is negligible in the starfish egg cell (Miyazaki et al., 1975 b). Therefore $V_0$ can be considered equal to the K equilibrium potential, $V_k$. It is likely that the major fraction of the membrane current is carried by K ions (Hagiwara and Takahashi, 1974; Miyazaki et al., 1975 b). Therefore, $g_\circ$ should represent the K conductance. The relationship between $g_\circ$ for the instantaneous current and $\Delta V$ calculated from Eq. 1 is shown in Fig. 3 A. The K conductance $g_\circ$ increases as $\Delta V$ becomes more negative and tends to saturate when $\Delta V$ exceeds $-40$ mV. On the other hand for positive values of $\Delta V$, $g_\circ$ becomes smaller as $\Delta V$ increases. The results demonstrate a clear inward-going rectification. Further, Fig. 3 A indicates that $g_\circ$ is not only a function of $\Delta V (= V - V_k)$ but also of the external K concentration. The dependence of $g_\circ$ on $[K^+]_o$ is demonstrated by calculating from the data presented in Fig. 3 A. The relative values of $g_\circ$ at 10, 25, 50, and 100 mM for a fixed $\Delta V$ are 1:1.7:2.3:3.0 for $\Delta V = -10$ mV, 1:1.7:2.5:3.3 for $\Delta V = -20$ mV, and 1:2.0:2.6:3.4 for $\Delta V = -30$ mV. The data indicate that the ratios are similar at different $\Delta V$'s for the range studied in the present work and that the ratios increase with $[K^+]_o$ substantially less sharply than expected from a linear relationship. In the present work,
however, no attempt was made to find out the form of function between $g_o$ and $[K^+]_o$. The values of $g_o$ at 10 and 25 mM K for $\Delta V = -30$ mV are 0.2 ~ 0.3 and 0.4 ~ 0.6 mmho/cm$^2$, respectively, when the surface area of the cell is calculated from its spherical shape.

**Time-Dependent K Current**

To examine the time-course of the time-dependent component, the difference between the actual current and its steady-state value $I_s$ was plotted against the time on a semilogarithmic plot (Fig. 3 B). The time-course is approximated satisfactorily by a single exponential curve. Therefore, the total membrane current $I(\Delta V \cdot t)$ may be expressed by:

$$I(\Delta V \cdot t) = I_d(\Delta V) - [I_d(\Delta V) - I_o(\Delta V)]e^{-t/\tau(\Delta V)},$$ (2)

where $I_o(\Delta V)$ is the instantaneous current seen at the onset of the voltage pulse.

![Figure 3](image)

**Figure 3.** (A) Relations between instantaneous K conductance $g_o$ and $\Delta V$ at four different K concentrations in Na-free media. (B) Log $(I - I_s)$ is plotted against time from the onset of voltage pulse. 25 mM K in Na-free solution. Holding potential at $V_o$ is $-49$ mV. The figure in each trace indicates magnitude of $\Delta V$. (C) Relationship of time constant, $\tau$ of current, and $\Delta V$ obtained at four different K concentrations in Na-free media. Data for A and C and those of Fig. 1 were obtained from the same experiment.

The time constant $\tau(\Delta V)$ is a function of $\Delta V$. For negative $\Delta V$ $\tau$ decreased as $\Delta V$ became more negative. The relationships between the logarithm of the time constant and $\Delta V$ at different external K concentrations are shown in Fig. 3 C. The time constant seems to be dependent on $V - V_K$ rather than either $V$ or $[K^+]_o$ alone. The time constant changes roughly exponentially as $\Delta V$ changes; a 10-fold decrease in the time constant is found with a negative shift of 45 ~ 55 mV in $\Delta V$. Time constants were not calculated precisely for positive $\Delta V$’s because of the small amplitude of the outward membrane current. The data suggest, however, that the time constant tended to decrease as $\Delta V$ increased.

The inward current tends to decline after reaching its maximum amplitude when $\Delta V$ is made more negative than $-40$ mV. A similar decline of the inward current has been found in the skeletal muscle fiber membrane (Adrian and
For large negative values of $\Delta V$ the decline tends to start earlier so that the determination of the value of $I_s$ is difficult (see Fig. 1, 10 mM K). Therefore, the analyses were limited generally to $\Delta V$'s of small amplitude (smaller than 40 mV). When a slight decline was present, the value of $I_s$ was assumed to be the maximum amplitude of the current. The decline found in the skeletal muscle fiber is considered to be due to the depletion of K ions in the external medium just outside the fiber membrane and is absent if the experiment is performed in isotonic K media. To determine whether the egg cell membrane behaved similarly, it was bathed in isotonic K solution (480 mM). However, the membrane conductance became so large that voltage clamp with microelectrodes became impossible. The mechanism of decline of the inward current will not be discussed in the present paper.

The current-voltage relations for the instantaneous current $I_o$ (curve I) and the steady-state current $I_s$ (curve II) obtained at 25 mM K (solution E) are shown in Fig. 4. As mentioned above, the relationship shows an inward-going rectification. For negative $\Delta V$, the amplitude of $I_s$ is larger than that of $I_o$. In contrast, when $\Delta V$ is positive, the amplitude of $I_s$ is smaller than that of $I_o$. The inward-
going rectification thus becomes more pronounced as the time-dependent current develops. The ratio \( I_d/I_o \) was calculated and plotted against \( AV \) (filled circles in Fig. 5 A). The ratio is unity at the holding membrane potential \( V_o \). It decreases with the increase of the positive \( AV \) and increases as the amplitude of the negative \( AV \) becomes greater, finally reaching a saturation value at \( AV < -40 \) mV. The maximum value of the ratio at the saturation level is denoted \( (I_d/I_o)_{\text{max}} \) and a dimensionless number \( n_o(\Delta V) \) is assigned to represent the normalized value of the ratio, i.e. \( n_o(\Delta V) = (I_d/I_o)_{\Delta V}/(I_d/I_o)_{\text{max}} \). Under this definition \( n_o \) is 1 at large negative \( \Delta V \)'s and decreases as \( \Delta V \) is made less negative. At \( V = V_o \) or \( AV = 0 \), \( n_o(0) = 1/(I_d/I_o)_{\text{max}} \) and this value is denoted by \( n_o \). The steady-state current \( I_d(\Delta V) \) is then expressed by

\[
I_d(\Delta V) = g_o(\Delta V) \cdot \frac{n_o(\Delta V)}{n_o} \cdot \Delta V.
\]

Here \( g_o(\Delta V) \) represents the instantaneous K conductance obtained when the membrane is equilibrated at \( V_o \). To use Eq. 3 to describe the entire time-course of the membrane current during the voltage clamp, \( n \) is made time dependent, and

\[
I(\Delta V,t) = g_o(\Delta V) \cdot \frac{n(\Delta V,t)}{n_o} \cdot \Delta V.
\]

\( g_o(\Delta V) \) in Eq. 4 is the same as that in Eq. 3, i.e. it has the dimension of conductance, it is an instantaneous function of \( \Delta V \) and is assumed to indicate the same \( g_o \) which was originally obtained when the membrane was equilibrated at \( V_o \). This also implies that \( g_o(\Delta V) \) does not depend on the previous history of the membrane potential. Eq. 4 thus assumes that the K conductance is expressed by a product of the time-independent and the time-dependent components. One simple physical model is the case in which each K channel shows an inward-going rectification represented by \( g_o(\Delta V) \). In such a model \( n \) represents the fraction of
open channel per unit membrane area. In the following two experiments the validity of Eq. 4 was examined.

In one experiment, the membrane potential was first clamped to \( \Delta V = -16 \text{ mV} \) and then shifted to various other potential levels at 0.11 or 1.15 s from the onset of the first pulse (Fig. 6 A). The instantaneous current voltage relations at 0.11 and 1.15 s just after the onset of the second pulse are illustrated by filled and open triangles in Fig. 4. The membrane current associated with the first pulse was already in the steady state at 1.15 s (Fig. 6 A) but it was still substantially smaller at 0.11 s. In the first step of \( \Delta V = -16 \text{ mV} \), \( I(\Delta V = -16 \text{ mV}, t = 0.11 \text{ s})/I_0(\Delta V = -16 \text{ mV}) \) and \( I(\Delta V = -16 \text{ mV}, t = 1.15 \text{ s})/I_0(\Delta V = -16 \text{ mV}) \) were 1.4 and 1.9, respectively. These values represent \( n/n_0 \) in Eq. 4 at 0.11 and 1.15 s after the onset of the pulse of \( \Delta V = -16 \text{ mV} \), since we assume any change in the membrane current during the maintained potential is due to a change in \( n \). If

\[ g_0(\Delta V) \text{ does not depend on the previous history of the membrane potential as assumed in Eq. 4 the instantaneous current voltage relations at 0.11 and 1.15 s should coincide with curves obtained by multiplying curve I by 1.4 and 1.9, respectively. The calculated curves are illustrated by dashed lines (III and IV in Fig. 4) and the result shows that this is the case.} \]

In the second experiment (Fig. 6 B) the amplitude of the second pulse was fixed to \( \Delta V_2 = -12 \text{ mV} \) and the amplitude of the first pulse, \( \Delta V_1 \), was varied. The duration of the first pulse was sufficiently long so that the membrane current had reached the steady-state level at the end of the pulse, i.e. \( n \) should have reached \( n_e \). Therefore, the amplitude of the current, \( I' \), just after the onset of the second pulse should be

\[ I' = g_0(\Delta V_2) \cdot \frac{n_e(\Delta V_1)}{n_e} \cdot \Delta V_2. \] (5)

If \( g_0 \) does not depend on the previous history of the membrane potential it
should always be \( g_o (\Delta V_2) \) and independent of \( \Delta V_1 \). In contrast the value of \( n \) at the onset of the second pulse should be almost equal to that at the end of the first pulse, as \( n \) requires time to change. When \( I' \) represents \( I' = g_o (\Delta V_2) \cdot \Delta V_2 \),

\[
I' = g_o (\Delta V_2) \cdot \Delta V_1 \tag{6}
\]

and then \( I'/I'' = n_o/n_o \). This indicates that \( I'/I'' \) vs. \( \Delta V_1 \) relation should coincide with the \( I_0/I_o \) vs. \( \Delta V \) relation since \( n_o/n_o = I_0/I_o \). The open circles in Fig. 5 A represent the actual data which agree with the \( I_0/I_o \) vs. \( \Delta V \) relation illustrated by filled circles. These results indicate that the entire membrane current can be described satisfactorily by Eq. 4.

Fig. 5 B shows \( I_0/I_o \) or \( n_o/n_o \) as a function of \( \Delta V \) obtained at four different K concentrations, and indicates that \( n_o \) as a function of \( \Delta V \) is independent of [K+]_o. This was also found for the time constant. Therefore, it is safe to conclude that

\[
\text{FIGURE 7. Effect of Cs}^+ \text{ upon the inward current of the membrane. Five traces of membrane currents at five different Cs concentrations (0, 0.03, 0.1, 0.3, and 1 mM) in 25 mM K, Na-free media. Those traces are superimposed for AV of the same magnitude indicated by figure above each family of membrane currents. Amplification for lower four families is different from that for upper ones. Holding potential, } -48 \text{ mV. Cell diameter, } 750 \mu\text{m.}
\]

the entire kinetics of \( n \) depend on \( V-V_K \), rather than either \( V \) or \([K^+]_o \) alone. When \( \Delta V \) becomes more negative than \(-40 \text{ mV} \) \( n_o \) reaches a saturation value. The average value of \( n_o/n_o \) at saturation obtained from the \( I_0/I_o \) vs. \( \Delta V \) relationship in 10 preparations was \( 2.3 \pm 0.1 \text{ (SD)} \). In other words, \( n_o = 0.43 \). This indicates that about 43% of the \( n \) process is already activated at \( V_o \) which is considered to represent \( V_K \).

**Blocking Effect of Cs on the K Channel**

Previously reported current clamp experiments (Hagiwara and Takahashi, 1974) demonstrated that \( Cs^+ \) does not carry significant membrane current but suppresses the \( K^+ \) current when added to \( K^+ \) media. Fig. 7 shows membrane currents obtained at 25 mM K in Na-free media. The five traces in each record were obtained with the denoted voltage pulse at \([Cs^+]_o \) concentrations 0, 0.05, 0.1, 0.3, and 1 mM. At these concentrations \( Cs^+ \) did not alter the resting potential. The records show how \( Cs^+ \) suppresses the inward current. For \( \Delta V = \)
-10 mV, no appreciable effect of Cs\textsuperscript{+} was observed. For more negative ΔV's (-19 and -28 mV) the Cs\textsuperscript{+} effect was significant at 1 and 0.3 mM, but was insignificant at lower concentrations. For large negative ΔV's (-64 and -73 mV) the suppressing effect was substantial even at 0.03 mM Cs. The result indicates, therefore, that the suppressing effect of Cs\textsuperscript{+} on the K\textsuperscript{+} inward current depends not only on the Cs\textsuperscript{+} concentration but also on the membrane potential.

The time-course of the inward current is often accelerated by Cs\textsuperscript{+}. In some cases such as those for ΔV = -73 mV at 0.3 and 0.1 mM Cs in Fig. 7 the initial instantaneous inward current is followed by a fast decline. This suggests that the suppression of the inward current by Cs\textsuperscript{+} requires time to develop after the membrane potential is altered. Since the suppression proceeds with time, this effect counteracts the time-dependent increase of the K current. The rapid decline requires that the time-dependent suppression overcome the time-dependent increase of the K current. To estimate the time-course of suppression, the membrane current obtained with Cs\textsuperscript{+} was normalized by dividing by the current obtained in the absence of Cs\textsuperscript{+} at the same time after the onset of the voltage pulse of the same ΔV. The results shown in Fig. 8 A were obtained with 0.3 mM Cs\textsuperscript{+} at different ΔV's and those in Fig. 8 B with various Cs\textsuperscript{+} concentrations at a fixed ΔV (-55 mV). The normalized current decreases with an approximately exponential time-course. The time constant tends to decrease as ΔV is made more negative for a given Cs\textsuperscript{+} concentration. When ΔV is fixed the time constant decreases as the Cs\textsuperscript{+} concentration increases. In other words the time-course of suppression tends to become faster when the steady-state suppression is greater.

The suppression generally reaches a steady-state level by 100 ms. Therefore, the membrane potential dependence of the Cs\textsuperscript{+} effect in the steady state was examined by observing the suppression of the membrane current 100 ms after the onset of the voltage pulse. Since the inward current starts to decline after reaching its maximum value when the amplitude of ΔV becomes greater, the membrane current deviates from that predicted by Eq. 1 as time progresses. However, when the current is observed at 100 ms from the onset of the pulse, this deviation is likely to be small even when ΔV is -80 mV. Fig. 8 C illustrates current-voltage relations at 100 ms after the onset of the voltage pulse obtained with 25 mM K in Na-free media. Data were obtained for seven different Cs\textsuperscript{+} concentrations. The amplitude of the current increases with increasing amplitude of the negative ΔV in the absence of Cs\textsuperscript{+}. When Cs\textsuperscript{+} is present, however, the current starts to decline at large negative ΔV's. Thus, the amplitude of the current reaches a maximum at a certain ΔV and a negative slope conductance region appears in the current-voltage relation. To analyze the membrane potential dependence of suppression, dose-response curves of Cs were constructed at various membrane potentials. The ratio x between the currents at 100 ms from the onset of the voltage pulse with and without Cs\textsuperscript{+} was plotted against logarithm of [Cs\textsuperscript{+}]\textsubscript{o} in Fig. 9 A. When the ratio is one, there is no suppression and if it is 0, the suppression is complete. Continuous curves were drawn according to the Michaelis-Menten equation with the assumption that Cs\textsuperscript{+} blocks the channel on a one-to-one basis. Using the appropriate dissociation constants, these curves fit
the experimental data fairly well. The dose-response curve is shifted along the concentration axis toward the left as \( AV \) is made more negative, i.e., the dissociation constant for Cs, \( K \), is membrane potential dependent. Fig. 9 B shows that the logarithm of \( K \) is linearly related to \( AV \). The slope indicates that \( K \) changes 10-fold for a change of 41 mV in the membrane potential. In two other experiments, the corresponding values were 38 and 40 mV, respectively. This indicates that the steady-state suppression by Cs\(^+\) at a fixed K\(^+\) concentration is a function of the product

\[
[\text{Cs}\,^+]_0 \, e^{\frac{-\alpha FAV}{RT}},
\]

(\( \alpha = 1.4-1.5 \)) rather than \( [\text{Cs}\,^+]_0 \) or \( AV \) alone.

The above results show that the suppressing effect of Cs\(^+\) depends on \( AV \)
when the Cs⁺ concentration is kept constant. In the experiment described above, however, the K⁺ concentration was kept at 25 mM throughout and, therefore, the result does not predict the behavior of the potential dependence when the K concentration is varied. If the suppression depends on V alone the same degree of suppression should occur at a given V when the K⁺ concentration is altered with a fixed Cs⁺ concentration. If, however, there is any competition between Cs⁺ and K⁺ for the same sites, the suppressing effect should decrease with an increase in [K⁺]o. There would be no cases in which the effect increases with the increasing [K⁺]o. In the experiment illustrated in Fig. 10 the effect of 0.5 mM Cs was examined at 10, 25, and 50 mM K. Three pairs of current-voltage relations in Fig. 10 A were obtained at 100 ms after the onset of the voltage pulse with (continuous lines) and without (dashed lines) Cs at three K concentrations. The ratio x between currents with and without Cs⁺ was plotted against V in Fig. 10 B. The value of x at a given V decreases as the K concentration increases, i.e., the blocking effect increases with the K concentration when compared at a fixed V. Thus it is unlikely that the suppressing effect of Cs depends on V alone. The dependence of the suppression upon \( V-V_K \) can be examined with the data in Fig. 10 B if each of three curves is shifted along the membrane potential axis so that three \( V_o's \) (indicated by arrows) coincide. For a given \( V-V_K \) at 10 mM K is always slightly smaller than x at 25 mM K which is always smaller than x at 50 mM K. In other words the blocking effect of Cs tends to decrease as the K concentration increases when compared at a fixed \( V-V_K \). Thus \( V-V_K \) alone does not determine the effect completely.

The potential-dependent suppression of the K⁺ current by Cs⁺ is at least in part, time dependent. The experimental results suggest that the instantaneous current is also affected. However, it is difficult to distinguish if the potential-dependent suppression of the instantaneous current at large negative \( \Delta V \) is due to the contamination by the early part of the time-dependent suppression. This problem was examined by observing currents during the recovery from the

![Figure 9](image-url)

**Figure 9.** (A) Dose-response curve for the suppression of Cs⁺ on the inward K current at \( \Delta V's \) of different magnitudes. Abscissa represents the ratio between currents with and without Cs calculated from the data in Fig. 8 C. Each continuous curve is derived from equation \( x = \frac{1}{1 + (\frac{[Cs\_o]}{K})^{-1}} \) with an appropriate dissociation constant, \( K \). (B). Logarithm of \( K \) is plotted as a function of \( \Delta V \).
potential-dependent suppression. The steady-state current-voltage relation obtained at 1 s after the onset of the voltage pulse in solution B (25 mM K) containing 0.5 mM Cs is shown in Fig. 11 A (dotted line with stars). The amplitude of the current becomes maximal at \( \Delta V = -40 \) mV and decreases as \( \Delta V \) is made more negative. The records in Fig. 11 B were obtained in the same experiment with a two-step voltage clamp. The membrane potential was kept at \( \Delta V = -81 \) mV for 1 s and then shifted to various second levels. The steady-state relation indicates that the current is suppressed considerably at \( \Delta V = -81 \) mV (indicated by an arrow in Fig. 11 A). When \( \Delta V \) at the second level is less negative than \( -81 \) mV the amplitude of the instantaneous current (filled circles in Fig. 11 A) obtained immediately after the onset of the second pulse is substantially smaller than that of the steady-state current. The amplitude of the current increases with time and eventually reaches the steady-state value. The current at 0.8 s after the onset of the second pulse was plotted against \( \Delta V \) of the second step.
in Fig. 11 A (open circles) and the plot coincided with the steady-state relation (stars). Since the n process of the K conductance should have reached a steady state by 1 s after the onset of the pulse, the time-course of the current during the second pulse represents the recovery from the potential-dependent suppression of Cs at more negative membrane potential. The time-course of the current is satisfactorily described by the single exponential function. The dashed line in Fig. 11 A represents the instantaneous current-voltage relation expected from Eq. 4 which describes the current in the absence of Cs⁺. The shape of the instantaneous current-voltage relation obtained with Cs⁺ in Fig. 11 A differs significantly from that expected without Cs⁺. The most likely explanation for

\[
\Delta V
\]

this discrepancy is that part of the recovery from the potential-dependent suppression is instantaneous. The recovery occurs probably in two steps. One is too fast to be resolved with the present technique and the other is slow and can be described as the first-order process.

**DISCUSSION**

The present experimental results show that the kinetics of the K current during the inward-going rectification in the starfish egg cell membrane differ in several ways from those of the K current of the squid giant axon described by Hodgkin and Huxley (1952). (a) The directions of rectification are opposite. (b) The kinetics depend on the membrane potential for the K⁺ current of the squid whereas they are determined by the electrochemical gradient of K ions, \( V - V_K \) in the inward-going rectification of starfish eggs. (c) The K conductance in the

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\text{FIGURE 11. (A) Current-voltage relations obtained in 25 mM K (solution B) containing 0.5 mM CsCl. Stars and dotted line represent steady-state relation obtained at 1 s after the onset of the voltage pulse. Circles were obtained from two-step voltage clamp experiment of the same preparation illustrated in B. Filled circles, the instantaneous current at the onset of the second pulse and open circles at 0.8 s after the onset of the second pulse. The broken line represents an instantaneous current-voltage relation expected in the absence of Cs when the steady-state current has the same magnitude. The first pulse (\( \Delta V = -81 \text{ mV} \)) lasted 1 s. The holding membrane potential, -49 mV. (B) Records of the two-step voltage clamp. The magnitude of \( \Delta V \) at the second voltage pulse is listed to the right of each current trace. Cell diameter, 750 \( \mu \text{m} \).} \]
squid axon is described in terms of \( g_k \cdot n^4 \) where \( g_k \) is a constant with the dimensions of conductance and \( n \) is a dimensionless number determined by two membrane potential-dependent rate constants \( \alpha_n \) and \( \beta_n \) via

\[
\frac{dn}{dt} = \alpha_n (1 - n) - \beta_n \cdot n. \tag{8}
\]

In the membrane of the starfish egg cell the K conductance is described in terms of \( g_k \cdot n \) where \( g_k \) which also has the dimensions of conductance is not a constant, but is an instantaneous function of \( V-V_K \). Thus, the \( K^+ \) conductance during the inward-going rectification follows the first-order kinetics while that of the squid axon membrane follows higher order kinetics. The rate constants \( \alpha_n \) and \( \beta_n \) and \( n \) in the egg cell membrane can be defined similarly by Eq. 8.

\[
\alpha_n = n_\infty / \tau. \tag{9}
\]
\[
\beta_n = (1 - n_\infty) / \tau. \tag{10}
\]

Since \( n_\infty \) and \( \tau \) are functions of \( V-V_K \), \( \alpha_n \), and \( \beta_n \) depend on \( V-V_K \) instead of \( V \). The calculated values of the rate constants at different \( V-V_K \)'s are shown in Fig. 12. They are much smaller than those found for the K current of the squid axon as would be expected from the slower time-course of the membrane current during the inward-going rectification in the starfish egg cell membrane.

The present results show that the K conductance during the inward-going rectification may be described as a product of two independent components. The one is an instantaneous function of \( V-V_K \) and the other depends on \( V-V_K \) as well as the time. As noted above the simplest interpretation of the results is to assume that each K channel has an inward-going rectification represented by the instantaneous conductance and therefore that \( n \) represents simply the density of the open channels. The inward-going rectification of the channel can be achieved if one assumes appropriate asymmetrical energy barriers in the channel (Woodbury, 1971). Another interpretation of the nonlinearity of the instantaneous current-voltage relationship would be to assume the existence of two time constants, one of which is too fast to be resolved by the present technique. Under this assumption the current-voltage relation of each membrane channel can be linear and the rectification could be explained in terms of an asymmetric effect of \( \Delta V \) on the opening and closing of the channels. In this case, the

![Figure 12. Rate constants \( \alpha_n \) and \( \beta_n \) are plotted against \( \Delta V \).](image-url)
rectification of the instantaneous response might be due to the fact that what is called "instantaneous" really represents a stage at which the process of opening (or closing) of the channels induced by the applied potential has already advanced to a considerable extent. The present experimental results do not distinguish between the above two cases. One way to do so would be to obtain knowledge on the current of a single channel, for example, through noise analysis. Our data on the instantaneous membrane current under the voltage clamp experiment is in good agreement with those in frog skeletal muscle fiber during inward-going rectification (Almers, 1971).

One of the particular features of the anomalous rectification is that the conductance change or the gating mechanism depends on $V-V_K$ rather than $V$ alone. A few different models have been proposed to explain this mechanism. Adrian (1969) and Horowicz et al. (1968) proposed carrier models. Armstrong (1975) explained the anomalous rectification with a channel model by assuming a blocking particle bound at the inner mouth of the channel. The removal of the blocking particle depends on the probability that the external K ions enter the channel close to the blocking site. The probability increases with an increase in the external K concentration as well as with an increase of membrane hyperpolarization. Thus, the opening of the channel depends on $V-V_K$. Baumann and Mueller (1974) proposed the following model to explain the alamethicin, monazomycin, or excitability-inducing material (EIM)-induced electrical excitability in lipid bilayers. In the absence of an electric field the channel-forming molecules lie at the surface of the membrane. An applied potential tilts them from the surface into the hydrocarbon region of the bilayer because of the dipole moment of the molecule. The tilted molecules form conducting channels and thus the gating mechanism becomes potential dependent. If one introduces the binding of the external K ions to such molecules as a necessary step for the molecule to acquire a dipole moment and therefore to tilt under the influence of the membrane potential, and if the internal K concentration is unaltered as in the present experimental conditions, the gating mechanism becomes dependent on $V-V_K$ rather than $V$ alone (personal communication by S. G. Ciani). The inward-going rectification can also be obtained by assuming carrier molecules with a dipole moment (personal communication by H. R. Guy).

The internal Cs$^+$ blocks the K channel of the squid giant axon and this effect is membrane potential dependent (Bezanilla and Armstrong, 1972). The blocking effect of Cs$^+$ on the K channel for the inward-going rectification in the starfish egg cell is also membrane potential dependent. There are, however, quantitative differences between the two cases. For the egg cell membrane the effective concentration of Cs$^+$ is lower than necessary for the squid axon membrane. Further, the suppression by Cs$^+$ in the K channel in the squid axon is instantaneous. In contrast, the suppression of Cs$^+$ on the conductance of the egg cell membrane is, at least in part, time dependent. In this respect the blocking effect of Cs$^+$ in the starfish egg cell resembles that of quaternary ammonium ions on the K$^+$ channel of the squid axon (Armstrong and Binstock, 1965; Armstrong, 1969, 1971). In a few experiments the effect of tetraethylammonium ions upon the inward K current of the starfish egg cell was examined. It has no effect even
in concentrations as high as 100 mM. These results suggest that the blocking sites of the two kinds of K channels may be different. Recently a similar potential-dependent blocking of the inward K current by external Cs ions in the squid axon has been found by French and Adelman (1975).

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