GALAXY MERGERS AS A SOURCE OF COSMIC RAYS, NEUTRINOS, AND GAMMA RAYS

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Received 2014 May 13; accepted 2014 June 27; published 2014 July 9

ABSTRACT

We investigate the shock acceleration of particles in massive galaxy mergers or collisions, and show that cosmic rays (CRs) can be accelerated up to the second knee energy ~0.1–1 EeV and possibly beyond, with a hard spectral index of \( \Gamma \approx 2 \). Such CRs lose their energy via hadronuclear interactions within a dynamical timescale of the merger shock, producing gamma rays and neutrinos as a by-product. If \( \sim 10\% \) of the shock dissipated energy goes into CR acceleration, some local merging galaxies will produce gamma-ray counterparts detectable by the Cherenkov Telescope Array. Also, based on the concordance cosmology, where a good fraction of the massive galaxies experience a major merger in a cosmological timescale, the neutrino counterparts can constitute \( \sim 20\%–60\% \) of the isotropic background detected by IceCube.

Key words: acceleration of particles – galaxies: evolution – neutrinos – shock waves

Online-only material: color figures

1. INTRODUCTION

The origin of cosmic rays (CRs), in particular above the knee energy \( \gtrsim 10^{16} \) eV and at ultra-high-energies (UHEs; \( \gtrsim 10^{19} \) eV), is still uncertain, but the discovery of sub-PeV neutrinos by IceCube (Aartsen et al. 2013, 2014; IceCube Collaboration 2013) may provide clues to this origin. Given that the distribution of the arrival directions is consistent with isotropy, most events are likely to come from extragalactic PeV accelerators (Murase et al. 2013, and references therein), although a fraction of them may be attributed to Galactic sources (e.g., Fox et al. 2013; Razzaque 2013; Ahlers & Murase 2013).

 Relevant constraints on the parent CR acceleration and the isotropic-neutrino-background (INB) production were given by Murase et al. (2013). They showed that if \( pp \) interactions are responsible for the INB, the parent CR spectrum must have a hard spectral index \( \Gamma \lesssim 2 \) in order for the by-product gamma rays not to overshoot the observed isotropic gamma-ray background (IGB; Abdo et al. 2010). Conversely, a significant fraction of the INB and the IGB may be attributed to a single type of source with a sufficiently hard spectral index. For this, the required local CR injection rate below the knee energies per energy decade is \( \varepsilon_{cr} Q_{cr} \sim 10^{44} \) min\(^{-1}\), where \( \varepsilon_{cr} \) is the effective hadronuclear optical depth at the source.

 Importantly, the above injection rate is comparable to that required for the UHECR sources \( \varepsilon_{cr} Q_{cr} \sim 0.5 \times 10^{44} \) erg Mpc\(^{-3}\) yr\(^{-1}\), or equivalently, the observed flux of the INB is consistent with the Waxman–Bahcall limit (Waxman & Bahcall 1999) with \( f_{pp} \sim 1 \). This may indicate that UHECRs also originate in the same type of sources (e.g., Katz et al. 2013). Note, however, that if indeed the parent CR spectrum of the INB is as hard as \( \Gamma \approx 2 \) and the maximum energy is in the UHE range, \( f_{pp} \) may have to become low at \( \gtrsim 10^{17} \) eV in order for the by-product neutrinos to be consistent with the non-detection of super-PeV neutrinos by IceCube (Laha et al. 2013).

 In summary, a significant fraction of the INB, the IGB, and possibly also the UHECRs, can be consistently attributed to a single type of source based on a \( pp \) scenario if:

 1. the sources have the right local CR injection rate of \( Q_{cr} \equiv \int d\varepsilon_{cr} Q_{cr} \gtrsim 10^{45} \) erg Mpc\(^{-3}\) yr\(^{-1}\),
 2. the sources accelerate CRs up to UHEs with a hard spectral index of \( \Gamma \lesssim 2 \), and
 3. the CRs with \( \lesssim 100 \) PeV lose a fraction of their energy via hadronuclear reactions, i.e., \( f_{pp} \sim 1 Q_{cr,45}^{-1} \).

(hereafter, we use \( Q_x = Q/10^x \)). Individual local source identifications using, e.g., HAWC (DeYoung & HAWC Collaboration 2012) and the Cherenkov Telescope Array (CTA; Actis et al. 2011) are the keys to testing the scenarios.

 Here, we investigate galaxy merger shocks (GMSs) as such a possibility. In the concordance cosmology, a good fraction of the massive galaxies experience a major merger and several minor mergers in a cosmological timescale. During the direct encounters between two galaxies, their cold-gas components are shocked with sufficiently large Mach numbers to enable an efficient CR acceleration. Below, we show that GMSs can meet the conditions (2) and (3), and the anticipated CR injection rate can be a good fraction of that required by condition (1) for a CR acceleration efficiency of \( \sim 10\% \).\(^1\)

2. GALAXY MERGER SHOCK SCENARIO

2.1. Energy Budget

First, let us estimate the intrinsic energy budget of a galaxy merger. Hereafter, we mainly consider major mergers between massive galaxies with a stellar mass of \( M_* \sim 10^{11} M_\odot \), which likely dominate the total energy budget. The energy dissipated by a GMS can be estimated as \( \mathcal{E}_{gms} \approx 0.5 M_{\text{gas}} v_s^2 \), or

\[
\mathcal{E}_{gms} \sim 2.5 \times 10^{58} M_{\text{gas},10^{11} M_\odot} v_s,7^2 \text{ erg,}
\]

where \( M_{\text{gas}} \) is the shocked gas mass and \( v_s \) is the shock velocity. At least up to \( z \sim 3 \), the galaxy gas mass is typically \( \sim 10\% \) of the stellar mass at the high-mass end with \( M_* \gtrsim 10^{11} M_\odot \) (e.g., Conselice et al. 2013). The shock velocity is essentially

\(^1\) We should note that the GMSs have been investigated as the source of UHECRs (e.g., Cesarsky & Ptuskin 1993; Jones 1998) and gamma rays (Lisenfeld & Völk 2010), separately.
the relative velocity between the merging galaxies, which can range up from \(v_s \sim (3-9) \times 10^5 \text{ cm s}^{-1}\) at a pericenter distance of \(R_{\text{gal}} \lesssim 1-10 \text{ kpc} \sim 3.1 \times 10^{21-22} \text{ cm}\) in the point particle approximation. The shock dissipation occurs with a dynamical timescale,

\[
t_{\text{dyn}} \approx R_{\text{gal}}/v_s \sim 20 R_{\text{gal},22.5} v_s,7.7^{-1} \text{ Myr},
\]

and the energy dissipation rate per merger is

\[
L_{\text{gms}} \sim 5.0 \times 10^{43} \xi_{\text{gms},58.5} v_s,7.7 R_{\text{gms},22.5}^{-1} \text{ erg s}^{-1}.
\]

The local major merger rate of massive galaxies has been estimated as \(R_{\text{gms}} \gtrsim 10^{-4} \text{ Mpc}^{-3} \text{ Gyr}^{-1}\) (e.g., Hopkins et al. 2010; Lotz et al. 2011). Equivalently, \(\gtrsim 10\%\) of massive galaxies experience major mergers in a cosmological time given that the mean density is \(n_{\text{gal}} \sim 10^{-2} \text{ Mpc}^{-3}\) (Bell et al. 2003). The possible CR injection rate by GMSs can be estimated as \(Q_{\text{cr,gms}} \approx \xi_{\text{cr}} F_{\text{gms}} R_{\text{gms}}\), or

\[
Q_{\text{cr,gms}} \sim 3.2 \times 10^{44} \xi_{\text{cr},-1} F_{\text{gms},58.5} R_{\text{gms},-4},
\]

where \(\xi_{\text{cr}}\) is the CR acceleration efficiency.

2.2. Cosmic-Ray Acceleration

Next, we consider the diffusive shock acceleration (DSA) mechanism (e.g., Drury 1983) at GMSs. For this, we consider first the characteristics of GMSs (see Figure 1). The Mach number of GMSs can be estimated as \(M \approx v_s/(5k_B T_s/3\mu)^{1/2} \sim 33 v_s,7.7 T_s,6.1^{1/2}\), which is much larger than unity for the cold gas component with \(T_s < 10^5 \text{ K}\). Here, we use \(\mu \approx 0.61 m_p\) for ionized gas (see below). On the other hand, the temperature downstream of the shock can be estimated as \(T_d \approx (3/16)(\mu v_s^2/k_B) \sim 3.4 \times 10^6 v_s,7.7^2 \text{ K}\). Such a high downstream temperature plays an important role in characterizing GMSs, first of all because the radiative cooling becomes relevant in this region. At \(T_d \gtrsim 10^6 \text{ K}\), the main cooling channel is provided by metal line emissions and free–free emission (e.g., Sutherland & Dopita 1993). Using an approximate form of the cooling function for a solar metallicity interstellar medium (ISM), the cooling timescale can be estimated as (Draine 2011)

\[
l_{\text{rad}} \approx 1.6 n_{\text{gas},0}^{-1} v_s,7.7^{17/5} \text{ Myr},
\]

where \(n_{\text{gas}}\) is the preshock gas density. From Equations (2) and (5), one can see that for a shock velocity \(v_s \lesssim 8.8 \times 10^5 R_{\text{gal},22.5}^{5/22} n_{\text{gas},0}^{5/22} \text{ cm s}^{-1}\), the downstream plasma cools within a dynamical timescale, i.e., the GMS shocks are radiative. In this case, a larger compression ratio than the \(\Gamma = 4\) ratio of strong adiabatic shocks is realized beyond the radiative region, which is

\[
l_{\text{rad}} \approx v_s/4 \times t_{\text{rad}} \sim 210 n_{\text{gas},0}^{-1} v_s,7.7^{22/5} \text{ pc}\]

from the shock surface. Such highly compressed regions are plausible sites for violent star formation during the galaxy merger (Larson & Tinsley 1978; Barnes 2004; Saitoh et al. 2009). Second, the UV photons from the radiative zone can significantly ionize the upstream ISM. Shull & McKee (1979) showed that this occurs for shock velocities \(v_s \gtrsim 10^8 \text{ km s}^{-1}\). In this case, one can naturally expect Alfvén-wave turbulence behind the GMS, which is crucial for the DSA mechanism. Large-scale magnetic fields in interacting galaxies are observed to be \(B \sim 10 \mu \text{G}\) (Drizgaza et al. 2011). One can also expect an amplification of the magnetic fields at least locally around the shocks as \(B \approx (4\pi \xi_B n_{\text{gas},0} m_p v_s^2)^{1/2}\), or

\[
B \sim 230 \xi_B^{-1/2} n_{\text{gas},0}^{1/2} v_s,7.7 \mu \text{G},
\]

where \(\xi_B \lesssim 1\) is the amplification factor.

In the DSA mechanism, the resultant CR spectral index, \(\Gamma\), where \(Q_{\text{cr}} \propto \xi_{\text{cr}}^{-1}\), is characterized by the compression ratio as \(\Gamma \approx (r + 2)/(r - 1)\) in the point-particle approximation. As discussed above, the compression ratio can be much larger than unity, \(r \gg 1\), comparing the upstream and the far downstream beyond the radiative zone. On the other hand, the size of the acceleration region in the downstream can be estimated as

\[
l_{\text{acc}} \approx D/v_s \sim 94 Z^{-1} \xi_B^{-1/2} n_{\text{gas},0}^{-1} v_s,7.7^{-2} \text{ cr}_{17,17} \text{ pc}.
\]

Here, \(D \approx c R_L/3\) is the diffusion coefficient in the Bohm limit, \(R_L = \xi_{\text{cr}}/Z e B \sim 0.47 Z^{-1} \xi_B^{-1/2} n_{\text{gas},0}^{-1} v_s,7.7^{-1} \text{ cr}_{17,17}\) is the Larmor radius, and \(Z\) is the electric charge of the CRs. From Equations (6) and (8), the CRs in the GMS acceleration reside in the region where \(r \approx 4\) for \(v_s \gtrsim 4.4 \times 10^7 \xi_B^{-5/6} n_{\text{gas},0}^{5/6} \text{ cm s}^{-1}\), and thus, the CR spectral index can be \(\Gamma \approx 2\).

The maximum energy possible for CRs is given by \(E_{\text{acc}} \approx t_{\text{acc}} = t_{\text{dyn}}\), where \(t_{\text{acc}} \approx \eta D/v_s^2\) is the acceleration timescale. This gives

\[
\xi_{\text{cr,max}} \approx \eta Z e B R_{\text{gal}} v_s/c,
\]

\[
\xi_{\text{cr,max}} \sim 3.5 \times 10^{18} \eta Z \xi_B^{-1/2} n_{\text{gas},0}^{-1/2} v_s,7.7^2 R_{\text{gms},22.5} \text{ eV}.
\]

Here, \(\eta\) depends on the effective compression ratio and the magnetic field configuration, etc. For an \(r = 4\) parallel shock in the Bohm limit, \(\eta = 3/20\). Thus, one can expect \(\xi_{\text{p,max}} \gtrsim 10^{17} \text{ eV}\) for proton CRs (\(Z = 1\)) at GMSs.

If highly efficient magnetic-field amplification, \(\xi_B \sim 1\), is the case at GMSs, the maximum energy could be further boosted.
up to UHEs for, e.g., iron CRs ($Z = 26$), which may be consistent with the possible transition in the Auger UHECR composition reported by (Abraham et al. 2010; but see also Abbasi et al. 2010). Note, however, that such UHECR fluxes can be suppressed by dissociation of the nucleus during the acceleration (Murase & Beacom 2010). Also, even proton CRs can be accelerated up to UHEs with larger GMS velocities as possible in galaxy collisions, $v_g \gtrsim 10^8$ cm s$^{-1}$, where the shocks are adiabatic. However, the size of the acceleration region of proton CRs with $\varepsilon_p \gtrsim 10^{17}$ eV can be larger than the width of the merging galaxy $\sim 0.1$–1 kpc (see Equation (8)). Then, a fraction of such CRs escape from the acceleration region, which also suppresses the UHECR flux.

### 2.3. Neutrinos and Gamma Rays

Next, let us discuss the energy loss of the CRs, which we have so far neglected, focusing on proton CRs in this section. When a GMS completes sweeping the galaxies, the high-pressure radiative region begins to cool down almost adiabatically, and so do the CRs trapped in this region. This occurs on a dynamical timescale, $t_dgm$ (Equation (2)). On the other hand, the energy loss timescale due to $pp$ interactions can be estimated as

$$t_{pp} \approx 1/\kappa_{pp} n_{gas} \sigma_{pp,c} \sim 26 n_{gas,0}^{-1} \text{Myr,}$$

(10)

where $\sigma_{pp} \sim 8 \times 10^{-26}$ cm$^2$ and $\kappa_{pp} \sim 0.5$ for $\varepsilon_{cr} = 10^{17}$ eV, and the cross section evolves only logarithmically with CR energy. The effective hadronuclear optical depth can be estimated as $f_{pp} = t_dgm/t_{pp}$, or

$$f_{pp} \approx 0.77 R_{gal,22.5} v_{r,7.7} n_{gas,0}^{-1}.$$  

(11)

Thus, CRs predominantly lose their energy via $pp$ interactions. Note that other energy loss processes, such as synchrotron, are irrelevant at least up to $\varepsilon_p \sim 10^{19}$ eV.

In $pp$ interactions, the charged and neutral pions are produced with a ratio of $\pi^- : \pi^0 \approx 2 : 1$. The charged pions finally decay into three neutrinos and one positron with roughly the same energy, and the neutral pions decay into two gamma rays. The flavor is totally mixed via neutrino oscillation for extragalactic sources. The spectral index of both the neutrinos and gamma rays is approximately the same as that of the parent protons, i.e., $\Gamma \approx 2.0$ in our case. The high energy cutoff is $\varepsilon_{\nu,\text{max}} \sim 0.05 \times \varepsilon_{p,\text{max}}/(1+z) \sim 4(1+z)^{-1} \varepsilon_{p,\text{max},17}$ PeV for neutrinos, and twice larger for gamma rays, although gamma rays above $\gtrsim 10$ TeV from $\gtrsim 100$ Mpc are attenuated by the extragalactic background light.

First, let us estimate the neutrino flux per flavor from a local GMS, that is, $\varepsilon_{\nu,i} \Phi_{\nu,i} \approx (1/6) \min[1, f_{pp}] \varepsilon_{\nu,i} L_{\text{gms}} / C (4\pi d_L^2)$, or

$$\varepsilon_{\nu,i} \Phi_{\nu,i} \sim 1.5 \times 10^{-13} \text{ erg cm}^{-2} \text{ s}^{-1} \text{ sr}^{-1} (18/C) (d_L/50 \text{ Mpc})^{-2} \times f_{pp} \varepsilon_{\nu,i} L_{\text{gms}} / C R_{gal,22.5}^{-1}.$$  

(12)

Here, $d_L$ is the luminosity distance to the source, and $C = \left(1 - (\varepsilon_{p,\text{max}} / \varepsilon_{p,\text{min}})^2 / (\Gamma - 2)\right)$ (or $C = \log(\varepsilon_{p,\text{max}} / \varepsilon_{p,\text{min}})$ for $\Gamma = 2$) is the bolometric correction factor. We take $\varepsilon_{p,\text{max}} = 10^{17}$ eV and $\varepsilon_{p,\text{min}} = \text{GeV}$ for the estimate. With the above parameter set, one can only expect a small muon event rate, $\sim 0.01$ yr$^{-1}$, using IceCube. Thus, individual local GMS source identifications through high-energy neutrinos will be difficult in the coming years.

![Figure 2](image_url)
The observed INB could be totally attributed to cosmological GMSs. The IGB flux can again be tightly connected to the INB flux as $\epsilon_\gamma^2 \Phi_\gamma \approx 2 \times 10^{-2} \Phi_{\nu_\gamma}^{\nu_\gamma=0.5}$. Following the same reasoning as in Murase et al. (2013), we see here that a fraction $>10\%$ of the observed IGB at $\sim 100$ GeV can be attributed to GMSs, for a slope of $\Gamma \approx 2.0$.

3. DISCUSSION

As we showed above, given the concordance cosmology and a CR acceleration efficiency of $10\%$, GMSs can provide at least $20\%–60\%$ of the observed INB. This scenario can be indirectly tested by detecting gamma rays from the local merging galaxies using CTA. Within the CTA detection horizon, $d_L \lesssim 100$ Mpc, one can expect $\Phi_{\gamma \gamma} \times t_{\text{dyn}} \times (4\pi d_L^{-3}/3) \lesssim 10$ such systems.

Two of the interesting candidates are the “Taffy” colliding galaxy pairs UGC 12914/5 and UGC 813/6 (Condon et al. 1993, 2002), located at $d_L = 60$ Mpc and 69 Mpc, respectively. In both cases, gas components of $\sim 10^{10} M_\odot$ collided with a velocity of $\sim 600$ km s$^{-1}$ a few 10 Myr ago. The bridge region between the galaxy pairs filled with shocked gases, and shows strong synchrotron emission which may come from non-thermal electrons accelerated by the GMS (Lisenfeld & Völk 2010). Another interesting candidate is VV 114 which is a gas-rich merging galaxy pair with a core separation of 6 kpc, located at $d_L \approx 77$ Mpc from the Earth (Soifer et al. 1987). The galaxy interaction may have already triggered the starburst and active galactic nucleus (AGN) activity in this system (Iono et al. 2004).

If the acceleration in GMSs is efficient, we can again expect $\sim 10$ local sources within the GZK radius $\lesssim 100$ Mpc, which might form hotspots in the UHECR sky. The number density of GMSs is smaller than the estimated number of sources required inside the GZK radius $>10^{3}$ (The Pierre Auger Collaboration 2013), but the flux from the merging galaxies could be $\sim 10\%$ of the observed one. Such UHECRs from local GMSs can arrive at the Earth on overlapping time windows with neutrinos and gamma rays for an intergalactic field of $<\text{NG}$ (e.g., Bhattacharjee 2000).

Finally, we should note that the GMS scenario is competitive with, but not easy to separate from, other scenarios. A fraction of starburst and AGN activities are triggered by galaxy mergers, as observed in VV 114. These latter activities can also inject a sufficient amount of CRs (e.g., Tamborra et al. 2014). An identification in terms of morphology is possible based on extensive computational simulations of merger histories. A more promising way to discriminate between the contributions from GMSs and those of starbursts may be to select for samples with relatively low far-infrared/radio flux ratios, which is observed in Taffy galaxies (Drzagza et al. 2011).

The authors thank the anonymous referee for valuable comments and Xuewen Liu, Kohta Murase, and Hidenobu Yajima for discussions. This work is supported by NASA NNX13AH50G.

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\[ \epsilon_{\gamma} > 0.1 \]