Search for the SUSY Electroweak Sector at $pp$ Colliders

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The sensitivity of future electron-proton colliders, the LHeC and FCC-eh, to weakly-produced supersymmetric particles is evaluated in this article. Supersymmetric scenarios where charginos ($\tilde{\chi}_1^\pm$) and neutralinos ($\tilde{\chi}_0^i$) are nearly degenerate in mass are considered. Two sets of models, which differ in the mass of sleptons ($\tilde{\ell}$), are studied. Under the hypothesis that slepton masses are at the multi-TeV scale (“decoupled” scenario), the production processes for charginos and neutralinos at $pp$ colliders, $p^- e^- \rightarrow j^- j^- \tilde{\chi}_1^\pm$ with $\tilde{\chi}_1^\pm = \tilde{\chi}_1^0$, $\tilde{\chi}_1^\mp$ or $\tilde{\chi}_2^0$, are considered. For the models where slepton masses are above but close to $\tilde{\chi}_1^0$, $\tilde{\chi}_2^0$ masses (“compressed” scenario), contributions from the processes $p^- e^- \rightarrow j^- j^- \tilde{\chi}_1^\pm$ and $j^- j^- \nu$ followed by the decays $\tilde{\chi}_1^\pm \rightarrow j^- j^+ e^-$ and $\nu \rightarrow j^- j^+ e^-$ are also taken into account. These scenarios are analysed with realistic detector performance, using multivariate techniques. Effects of systematic uncertainties and electron beam polarization dependence are also discussed. The reach is found to be complementary to the one obtained at $pp$ colliders, in particular for the compressed-slepton scenario.

I. INTRODUCTION

Supersymmetry (SUSY) is one of the most promising new physics scenarios beyond the Standard Model (SM). It has been explored widely in various production and decay channels at the Large Hadron Collider (LHC). Due to the large production cross sections in strong interactions at $pp$ colliders, the current LHC experiments have produced impressive constraints on the SUSY coloured sector (squarks and gluinos), excluding masses up to approximately 2 TeV at a centre-of-mass energy of $\sqrt{s} = 13$ TeV by the CMS collaboration with integrated luminosity of 137 fb$^{-1}$ [1] and by the ATLAS collaboration with 139 fb$^{-1}$ integrated luminosity [2].

Because of their much lower direct production cross sections, less stringent constraints have been placed on weakly-produced SUSY particles, namely neutralinos $\tilde{\chi}_0^i$, charginos $\tilde{\chi}_1^\pm$, and sleptons $\tilde{\ell}^\pm$. Here, $\tilde{\chi}_0^0$ and $\tilde{\chi}_1^\pm$ (collectively referred to as electroweakinos) are the SUSY partners of the Higgs and gauge bosons described in the mass eigenstates. If R-parity is conserved, the lightest neutralino $\tilde{\chi}_1^0$ can be the lightest SUSY particle (LSP) and a candidate for dark matter.

A variety of searches for $\tilde{\chi}_1^\pm$, $\tilde{\chi}_2^0$, and $\tilde{\ell}^\pm$ at $\sqrt{s} = 13$ TeV have been reported by the ATLAS [4] and CMS [5,15] collaborations with 36 fb$^{-1}$ of integrated luminosity. Recently, the collaborations have updated the analyses with up to 139 fb$^{-1}$ integrated luminosity [16–21]. Most of the studies target the processes $pp \rightarrow \tilde{\chi}_1^\pm \tilde{\chi}_2^0 \rightarrow W^\pm Z \tilde{\chi}_1^0 \tilde{\chi}_1^0$ and $pp \rightarrow \tilde{\ell}^+ \tilde{\ell}^- \rightarrow l^+ l^- \tilde{\chi}_1^0 \tilde{\chi}_1^0$, exploiting events characterized by multiple charged leptons and large missing transverse momentum, $E_T$. Dedicated searches for decays through the Higgs boson ($pp \rightarrow \tilde{\chi}_1^\pm \tilde{\chi}_2^0 \rightarrow W^\pm h \tilde{\chi}_1^0 \tilde{\chi}_1^0$) are also performed. Searches for electroweakinos decaying through sleptons exclude masses above 1 TeV (see for example [5]). Lower bounds of $\mathcal{O}(100)$ GeV on $\tilde{\chi}_1^\pm / \tilde{\chi}_2^0$ masses are obtained, depending on the scenarios; for example, Ref. [6] excludes $\tilde{\chi}_1^\pm / \tilde{\chi}_2^0$ decaying via $W^\pm$ and $Z$ bosons up to approximately 600 GeV with 95% confidence level (CL), while Ref. [21] reports that the left-handed selectron $\tilde{e}_L$ masses can be excluded up to approximately 550 GeV. These limits mostly apply to scenarios characterised by a large mass difference, $\Delta m$, between $\tilde{\chi}_1^0$ and the next lightest supersymmetric particle (NLSP), either $\tilde{\chi}_1^\pm / \tilde{\chi}_2^0$ or $\tilde{\ell}^\pm$. In the case of small mass differences (e.g., $1$ GeV $< \Delta m < 50$ GeV, with $\Delta m$ still sufficiently large to guarantee prompt $\tilde{\chi}_1^\pm / \tilde{\chi}_2^0$ decays), $W^\pm$ and $Z$ bosons are off-shell and scenarios are referred to as “compressed”: the visible decay products from $\ell$ and $\tilde{\chi}_1^\pm / \tilde{\chi}_2^0$ have very soft transverse momenta ($p_T$) and the SM backgrounds are kinematically similar to the signal. The analyses therefore become challenging and sensitivities decrease substantially.

Dedicated searches have been recently developed by the LHC experiments to target low-$\Delta m$ scenarios. They exploit the recoil of the sparticles system against an initial state radiation (ISR) jet for efficient detection of soft decay products. Assuming $\Delta m \sim 5$ GeV, the ATLAS collaboration has excluded $\tilde{e}_L$ masses up to around 160 GeV and $\tilde{\chi}_1^\pm / \tilde{\chi}_2^0$ masses up to around 200 GeV [17]. A similar reach has been reported by the CMS collabora-
tion \cite{12}, as well as searches exploiting vector-boson fusion (VBF) production \cite{15}. Phenomenological studies on weakly-produced SUSY particles in compressed scenarios have been also reported in Refs. \cite{22, 31}.

Studies on the potential of the high-luminosity LHC (HL-LHC) \cite{32}, which foresees 3 ab$^{-1}$ of data taken at a centre-of-mass energy of 14 TeV, have shown that searches for low-momentum leptons and ISR-jet boost will be sensitive to chargino masses up to 400 (350) GeV for $\Delta m(\tilde{\chi}_1^+/\tilde{\chi}_2^0, \tilde{\chi}_1^0) \sim 5$ GeV, and to mass splittings between 1 and 50 GeV, assuming Wino-like (Higgsino-like) cross sections for electroweakino productions. Similar search techniques can also be used to target pair produced sleptons in compressed scenarios. It is worth noting that, to suppress SM backgrounds, analyses targeting very small $\Delta m$ require soft-momentum leptons from the decays of the sleptons, charginos or neutralinos and are thus complementary to searches targeting very large $\Delta m$ via multiple high-$p_T$ leptons. Regions of intermediate $\Delta m(\tilde{\chi}_1^+/\tilde{\chi}_2^0, \tilde{\chi}_1^0) \sim 20-50$ GeV may still be elusive after the HL-LHC.

This article focuses on compressed electroweakinos scenarios, produced assuming Wino-like cross sections and mass differences between $\tilde{\chi}_1^+, \tilde{\chi}_2^0$ and $\tilde{\chi}_1^0$ small, $\mathcal{O}$(GeV), but still allowing their prompt decay. Two SUSY scenarios with different hypotheses on the charged slepton masses are considered to evaluate the sensitivity of future ep colliders, the Large Hadron electron Collider (LHeC) and the electron-hadron mode of the Future Circular Collider (FCC-eh), to discover SUSY electroweakinos and sleptons. The search uses the multivariate analysis approach (MVA) and Monte Carlo (MC) generated events passed through a realistic detector-level simulation. The electron and proton beam energies are assumed to be 60 GeV × 7 TeV (60 GeV × 50 TeV) at the LHeC (FCC-eh), which correspond to $\sqrt{s} = 1.3$ TeV (3.5 TeV). The maximal integrated luminosity at the LHeC is expected to be 1 ab$^{-1}$, while it could reach 2.5 ab$^{-1}$ at the FCC-eh after a 25-year running period. The centre-of-mass energy, $\sqrt{s}$, of ep colliders are considerably lower than the HL-LHC. However, since there are no gluon-exchange diagrams, the SM QCD backgrounds, which are dominant at pp colliders, are much smaller. Furthermore, the number of additional interactions in the same event (pile-up) is negligible at ep colliders, whilst it is expected to be very large at the HL-LHC. Previous studies on Higgsino-like $\tilde{\chi}_0^0/\tilde{\chi}_1^\pm$ production at ep colliders can be found in Ref. \cite{33, 34}, where Ref. \cite{33} focus on decoupled-scenarios and assume an optimistic electron beam energy of 140 GeV paired to 7 TeV and 50 TeV protons, while Ref. \cite{34} explores the parameter space for long-lived Higgsinos.

The article is organised as follows. Sec. II presents the SUSY scenarios considered. In Sec. III data simulation, signal and background processes and search strategy are reported. In Sec. IV the results of the compressed-slepton scenario are presented. The results of the decoupled-slepton scenario are reported in Sec. V. Conclusions and discussions on the effects of electron beam polarizations are presented in Sec. VII.

**II. SUSY SCENARIOS**

![FIG. 1. Some representative production diagrams for the signal processes considered in this article. The decoupled-slepton scenario includes only the upper two diagrams, while the compressed-slepton scenario includes both the upper and lower diagrams.](image)

Two SUSY compressed scenarios with different hypotheses on the charged slepton masses are considered. In the first scenario, referred to as the “decoupled-slepton” scenario, we assume that the only SUSY particles within kinematic reach are the electroweakinos $\tilde{\chi}_1^0$ and $\tilde{\chi}_1^\pm$. The LSP $\tilde{\chi}_1^0$ is assumed to be Bino-like, the $\tilde{\chi}_2^0$ and $\tilde{\chi}_2^\pm$ are Wino-like and degenerate in masses, and the mass difference between $\tilde{\chi}_1^0$ and $\tilde{\chi}_1^\pm$ is small ($\Delta m \sim 1$ GeV). All other SUSY particles are at the multi-TeV scale and therefore decoupled. The upper two diagrams in Fig. 1 represent the typical production processes in this scenario: charginos and neutralinos are produced via VBF processes. This scenario is motivated by dark matter coannihilation arguments \cite{35, 38}. For a Bino-like dark matter, the annihilation cross section is usually too low. The Wino-like $\tilde{\chi}_1^+/\tilde{\chi}_2^0$ with masses of order 1-10 of GeV larger than the LSP enhance the coannihilation processes, which may result in the dark matter relic density consistent with observations. In the second scenario, referred to as “compressed-slepton” scenario, the left-handed charged sleptons $\ell^+_L$ and sneutrinos $\tilde{\nu}_L$ are assumed to be kinematically accessible and slightly heavier than $\tilde{\chi}_1^+/\tilde{\chi}_2^0$. The signal production in this case includes both the upper and lower diagrams in Fig. 1. This scenario is also motivated by coannihilation arguments \cite{49}. Furthermore, since the main SUSY contributions to the muon anomalous magnetic moment, $(g-2)_\mu$, are given by the neutralino-muon and chargino-sneutrino loop diagrams, SUSY mass spectra containing neutralinos and sleptons of mass $\mathcal{O}(100)$ GeV may explain the discrep-
In the decoupled-slepton scenario, since the charged sleptons and sneutrinos $\tilde{\nu}$ are at the multi-TeV scale, signal events $p e^- \to e^- \tilde{\chi}_1^- \tilde{\chi}_1^0$ are produced via VBF processes of charginos and neutralinos only (c.f. upper two diagrams in Fig. 1). In the compressed-slepton scenario, however, since the left-handed slepton $\tilde{l}_L$ and $\tilde{\nu}$ are slightly heavier than the $\tilde{\chi}_1^\pm$ and $\tilde{\chi}_2^0$, the signal events $p e^- \to e^- \tilde{\chi}_1^- \tilde{\chi}_1^0$ include not only VBF processes of $\tilde{\chi}_1^\pm$ and $\tilde{\chi}_2^0$ but also the direct production of $\tilde{e}_L$ and $\tilde{\nu}$ followed by the decays of $\tilde{e}_L \to \tilde{\chi}_2^0 + e^-$ and $\tilde{\nu} \to \tilde{\chi}_1^+ + e^-$ (i.e. $p e^- \to j \tilde{e}_L \tilde{\nu} \to j e^- \tilde{\chi}_1^- \tilde{\chi}_1^0$). Thus both the upper and lower diagrams in Fig. 1 contribute to the signal rate in the compressed-slepton scenario.

Simulated data are generated at parton-level by MadGraph5_aMC@NLO 2.4.3 by importing the general MSSM model with the model parameter file prepared by the SUSY-HIT package [43]. Pythia performs parton showering and hadronization, and Delphes [44] is used for detector simulation. The detectors at $e^+ e^-$ colliders are assumed to have a cylindrical geometry comprising a central tracker followed by an electromagnetic and a hadronic calorimeter. The forward and backward regions are also covered by a tracker, an electromagnetic and a hadronic calorimeter. The angular acceptance of charged tracks and the detector performance in terms of momentum and energy resolution of electrons, muons, and jets are based on the LHeC (FCC-eh) detector design [45,46]. In particular, electrons are selected in the pseudorapidity range of $-4.3 < \eta < 4.9$ ($-5.0 < \eta < 5.2$) at the LHeC (FCC-eh), while jets are selected within an $\eta$ range between $\pm 5$ for the LHeC and $\pm 6$ for the FCC-eh. For the simulation, a modified Pythia version tuned for the $e^+ e^-$ colliders and the Delphes card files for the LHeC and FCC-eh detector configurations [47] are used.

Due to the presence of large missing transverse momentum in the final state, processes with production of neutrinos will contribute to the SM background. We separate the background into two categories: the 2-neutrino process $p e^- \to j e^- \nu \nu$ and the 1-neutrino process $p e^- \to j e^- \ell \nu$, where $\nu$ stands for the neutrino and anti-neutrino with all flavors of $e, \mu, \tau$. The 2-neutrino process has the same final state as the signal and is an irreducible background. The 1-neutrino process has a large cross section and will therefore have a non-negligible contribution to the background if one of the two leptons is undetected.

The following pre-selections are applied for LHeC (FCC-eh, reported if differing) studies:

1. At least one jet with $p_T > 20$ GeV, $|\eta| \leq 5.0 (6.0)$;
2. Exactly one electron with $p_T > 10$ GeV, $-4.3 < \eta < 4.9$ ($-5.0 < \eta < 5.2$);
3. No b-jet with $p_T > 20$ GeV;
4. No muon or tau with $p_T > 10$ GeV;
5. Missing transverse momentum $E_T > 50$ GeV.

After the pre-selections, 17 observables listed in the following are used as inputs to the TMVA package [48] to perform a multi-variant analysis through a boost decision tree (BDT) approach.

1. Global observables:
   1.1. the missing transverse momentum $E_T$;
   1.2. the scalar sum of $p_T$ of all jets, $H_T$.
2. Observables for the visible objects:
2.1. $p_T$ and the pseudorapidity $\eta$ of the first leading jet $j_1$ and the first leading electron $e_1$: $p_T(j_1), \eta(j_1), p_T(e_1), \eta(e_1)$;  
2.2. the pseudorapidity difference $\Delta \eta$ and the azimuthal angle difference $\Delta \phi$ between $j_1$ and $e_1$: $\Delta \eta(j_1, e_1), \Delta \phi(j_1, e_1)$;  
2.3. the invariant mass $M$, $p_T$ and $\eta$ reconstructed from the 4-vector of the system of $j_1$ and $e_1$: $M(j_1 + e_1), p_T(j_1 + e_1), \eta(j_1 + e_1)$.

3. Angular correlations between the missing transverse momentum and visible objects:

3.1. $\Delta \phi$ between $E_T$ and $j_1$, $e_1$, or $j_1 + e_1$: $\Delta \phi(E_T, j_1), \Delta \phi(E_T, e_1), \Delta \phi(E_T, j_1 + e_1)$;  
3.2. the transverse mass $M_T$ of the system of $E_T$ and $j_1$, $e_1$, or $j_1 + e_1$: $M_T(E_T, j_1), M_T(E_T, e_1), M_T(E_T, j_1 + e_1)$.

The BDT score for each event is used to separate the signal events from the SM background. The BDT threshold value is optimized for each SUSY scenario as well as for each collider, since kinematical distributions might vary as a function of $m_{\tilde{\chi}_1^\pm, \tilde{\chi}_2^0}$ and the beam energies. The number of signal and background events passing the BDT selection, $N_s$ and $N_b$, are used to calculate the significance. Assuming no systematic uncertainty, the statistical significance, $\sigma_{\text{stat}}$, of the potential signal is evaluated as

$$\sigma_{\text{stat}} = \sqrt{2[(N_s + N_b)\ln(1 + \frac{N_s}{N_b}) - N_s]}. \quad (1)$$

Including a systematic uncertainty $\sigma_b$ in the evaluation of the number of background events, the significance is given by

$$\sigma_{\text{stat+sys}} = \left[2\left((N_s + N_b)\ln \frac{(N_s + N_b)(N_b + \sigma_b^2)}{N_b^2 + (N_s + N_b)\sigma_b^2} - \frac{N_s}{\sigma_b} \ln \left[1 + \frac{\sigma_b^2 N_s}{N_b(N_b + \sigma_b^2)}\right]\right)\right]^{1/2}. \quad (2)$$

IV. COMPRESSED-SLEPTON SCENARIO

The compressed-slepton scenario is characterised by three sets of masses, which are

$$m_{\tilde{\ell}_L}, m_{\tilde{\chi}_1^\pm, \tilde{\chi}_2^0}, m_{\tilde{\chi}_1^0} \quad (3)$$

in the descending order, where $m_{\tilde{\ell}_L}$ represents the mass of charged sleptons, here assumed dominated by the left-handed component, or sneutrinos. In this article, we assume nearly degenerate electroweakinos, with $m_{\tilde{\chi}_1^\pm, \tilde{\chi}_2^0} = m_{\tilde{\chi}_1^0} + 1$ GeV, and prompt $\chi_1^\pm, \chi_2^0$ decays. The mass splitting between $\tilde{\ell}_L$ and $\tilde{\nu}$ is generally below 10 GeV for tan $\beta$ between 3 and 40. In this study, the benchmark $\tan \beta = 30$ is assumed, which results in the mass difference between $\tilde{\ell}_L$ and $\tilde{\nu}$ of around 9 GeV.

In this section, the $\Delta m$ symbol is used to denote the mass difference between the $\ell$ and $\chi_1^\pm, \chi_2^0$, i.e.

$$\Delta m = m_{\tilde{\ell}} - m_{\chi_1^\pm, \chi_2^0}. \quad (4)$$

A. Results with fixed $\Delta m$

We first discuss the case with $\Delta m = 35$ GeV, where 35 GeV is used as a proxy for intermediate-low-$\Delta m$ scenarios. The branching ratios for sleptons are $BR(\tilde{\ell}_L \rightarrow \chi_{1,2}^0 + e^-) \approx 40\%$ and $BR(\tilde{\nu} \rightarrow \chi_{1,2}^0 + e^-) \approx 60\%$. The other decay channels, $\tilde{\ell}_L \rightarrow \nu + e$ and $\tilde{\nu} \rightarrow \chi_2^0 + e^-$, have no electrons in the final state (except for very soft sleptons), and therefore will not contribute to the signal.

![BDT plot](image)

**FIG. 3.** Distributions of BDT response at the FCC-eh (upper) and the LHeC (lower) with the unpolarized electron beam for signal $j e^- \tilde{\chi}$ (black with filled area) in the compressed-slepton scenario, and the SM background of the $j e^- \nu\nu$ (red) and $j e^- l\nu$ (blue) processes after applying the pre-selection cuts. For signals, $m_{\chi_1^\pm, \chi_2^0} = 400$ GeV and 250 GeV at the FCC-eh and LHeC, respectively.

Figure [9] of the Appendix shows kinematic distributions of the input observables, both for signal and background, for the FCC-eh case assuming an unpolarized electron beam ($P(e^-)=0$). A SUSY model with $m_{\chi_1^\pm, \chi_2^0} = 400$ GeV and production $e^- p \rightarrow j e^- \tilde{\chi}$ is assumed, while the two sources of SM backgrounds, $e^- p \rightarrow j e^- \nu\nu$ and $j e^- l\nu$, are shown separately. Distri-
The number of events at each selection stage is shown in Table I, which corresponds to an integrated luminosity of 1 ab$^{-1}$. The optimized value for the BDT is found to be 0.262 for this SUSY model. Assuming a systematic uncertainty of 5%, i.e., $\sigma_b = 0.05N_b$, the number of events after the optimized BDT cut, $N_s = 149$ and $N_b = 686$, results in a significance of $\sigma_{\text{stat+syst}} = 3.3$. The 5% systematic uncertainties on SM backgrounds are assumed to include experimental sources (e.g., jet energy scale and resolution, lepton identification) and modelling uncertainties (renormalisation and factorisation scale choices, PDF). They are expected to be constrained by semi data-driven techniques and improved Monte Carlo predictions and the 5% value is assumed on the basis of a conservative extrapolation of uncertainties estimated in $pp$ monojet prospect studies at HL-LHC [49].

![Image](image-url)

TABLE I. Number of events after selections applied sequentially on SUSY signal $j e^- \tilde{\chi}^0$ with $m_{\tilde{\chi}^0} = 400$ GeV in the compressed-slepton scenario, and for the SM background processes of $j e^- \nu \nu$ and $j e^- \ell \nu$. The numbers of events correspond to an integrated luminosity of 1 ab$^{-1}$ at the FCC-eh with unpolarized electron beam. The significances including 5% systematic uncertainties on the background are presented in the last row.

| LHeC [1 ab$^{-1}$] | Signal | Background |
|---------------------|--------|------------|
| $m_{\tilde{\chi}^i}$ [GeV] | 250 | $j e^- \nu \nu$ |
| $m_{\tilde{\nu}}$ [GeV] | 285 | $j e^- \ell \nu$ |
| initial | 1251 | $2.80 \times 10^3$ |
| Pre-selection | 453 | $6.60 \times 10^3$ |
| BDT $> 0.172$ | 49 | 486 |
| $\sigma_{\text{stat+syst}}$ | 1.0 | 278 |

The same analysis is performed for the LHeC case, where we assume $m_{\tilde{\chi}^i, \tilde{\chi}^0} = 250$ GeV as the benchmark masses. The distributions of input observables are shown in Fig. [10] and the BDT-score distribution is reported in the lower panel of Fig. [3]. The cut flow is given in Table II, where the optimized BDT cut of 0.172 is used. Considering an integrated luminosity of 1 ab$^{-1}$ and 5% systematic uncertainty on the background, the significance of about 1.0 is obtained for this benchmark point.

![Image](image-url)

FIG. 4. Significances as varying the masses of $\tilde{\chi}^\pm$ and $\tilde{\chi}^0$ for the compressed-slepton scenario. Upper plot: at the FCC-eh with unpolarized beams and integrated luminosities of 1 ab$^{-1}$ and 2.5 ab$^{-1}$; Lower plot: at the LHeC with unpolarized beams and 1 ab$^{-1}$ luminosity. For dashed (solid) curve, a systematic uncertainty of 0% (5%) on the background is considered.

In the upper panel of Fig. [10] the significance curves as a function of $m_{\tilde{\chi}^\pm, \tilde{\chi}^0}$ for the FCC-eh with unpolarized electron beam and integrated luminosities of 1 ab$^{-1}$ and 2.5 ab$^{-1}$ are presented. With 0% (5%) systematic uncertainty on the background and 2.5 ab$^{-1}$ integrated luminosity, the 2-$\sigma$ limits on the $\tilde{\chi}^\pm, \tilde{\chi}^0$ mass are 616 (466) GeV, while the 5-$\sigma$ discovery limits are 517 (367) GeV.

The lower panel of Fig. [10] shows the significance curves at the LHeC with unpolarized electron beam and an integrated luminosity of 1 ab$^{-1}$. With 0% (5%) systematic uncertainty on the background, the limits on the mass are 266 (224) GeV and 227 (187) GeV corresponding to the 2 and 5-$\sigma$ significances, respectively.

1 In case the $\eta$ range of the jet is restricted to $\pm 5.5$, equivalent to a less-than-ideal calorimeter coverage at the FCC-eh, both the signal and background rates are reduced by less than 5%, and the significance is only slightly reduced.
B. Effects of Varying $\Delta m$

The effect of varying the assumption on $\Delta m$ is evaluated. A range between 5 to 65 GeV is considered, with $m_{\tilde{\chi}^\pm_1,\tilde{\chi}_2^0}$ being fixed at 400 GeV\(^2\). The distributions of the BDT response at the FCC-eh for different $\Delta m$ assumptions are presented in Fig. 5. Although the same background is analyzed, the BDT distributions change for different $\Delta m$ assumptions, because the signal kinematics varies with $\Delta m$ values. As $\Delta m$ increases, the kinematics of the 2-neutrino background $j e^- \nu\nu$ becomes similar to that of the signal process $j e^- \tilde{\chi}_1^\pm \tilde{\chi}_1^- \tilde{\chi}_1^0$ which renders its BDT distribution largely overlapping with that of the signal. When $\Delta m > 35$ GeV, part of the 1-neutrino background $j e^- \ell\nu$ events also begins to mimic the signal. Because of clearer distinctions between the BDT distributions of the signal and background, the BDT is most effective in rejecting the SM background if $\Delta m$ between 10 and 40 GeV.

The significances assuming either 5% or 0% systematic uncertainties on the background as a function of the mass difference $\Delta m = m_{\tilde{\ell}} - m_{\tilde{\chi}^\pm_1,\tilde{\chi}_2^0}$ when fixing electroweakino masses, $m_{\tilde{\chi}^\pm_1,\tilde{\chi}_2^0} = 400$ GeV, in the compressed-slepton scenario at the FCC-eh.

GeV can be tested with maximum efficiency. This is because, as shown in Fig. 5 for small $\Delta m$, the BDT distributions present a better separation between signal and background. However, when $\Delta m << 20$ GeV, the electron from the slepton and sneutrino decays become too soft to pass the pre-selections, $p_T(e^-) > 10$ GeV, suppressing the signal number of events.

It is worth noting that, although the significances for $\Delta m = 12$ and 5 GeV are slightly lower than $\Delta m = 20$ GeV, when 5% systematic uncertainty on background is included, they are still larger than the benchmark case with $\Delta m = 35$ GeV. However, when no systematic uncertainty on background is considered, $\Delta m = 35$ GeV gives larger significance compared to $\Delta m = 12$ and 5 GeV. Overall, significances are quite sensitive to the assumption of systematic uncertainty when $\Delta m > 20$ GeV. Therefore, to enhance the discovery potential to the SUSY electroweak sector, it will be important to control the level of systematic uncertainties on the background.

V. DECOUPLED-SLEPTON SCENARIO

In the decoupled-slepton scenario, where the sleptons are assumed to have multi-TeV mass, the signal events are mainly arising from the VBF processes of charginos and neutralinos, $pe^- \rightarrow j e^- e^+ e^-\tilde{\chi}_1^- \tilde{\chi}_1^0$. As this is a four-body production process, the signal cross sections are considerably lower than in the case of compressed-slepton scenario (cf. Fig. 2). At the LHeC they are of the order of 1 fb or lower, hence the decoupled-slepton scenario is only considered for the FCC-eh case.

As in the previous section, the kinematic distributions of input observables for events passing the pre-selections are shown in Fig. 11 in the Appendix A, where the signal events are from the process $pe^- \rightarrow j e^- \tilde{\chi}_1^- \tilde{\chi}_1^0$ with $m_{\tilde{\chi}^\pm_1,\tilde{\chi}_2^0} = 250$ GeV and the SM backgrounds are from of $j e^- \nu\nu$ and $j e^- \ell\nu$. The corresponding BDT-inputs distributions are presented in Fig. 11 Table III shows the number of events after each selection is applied sequen-

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\(^2\) When $\Delta m < 9$ GeV, $\tan\beta$ is changed from 30 to smaller value such that the LSP can still be $\tilde{\chi}_1^0$, rather than $\tilde{\nu}$. 

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FIG. 5. Distributions of the BDT response when fixing $m_{\tilde{\chi}^\pm_1,\tilde{\chi}_2^0} = 400$ GeV and varying the mass difference $\Delta m = m_{\tilde{\ell}} - m_{\tilde{\chi}^\pm_1,\tilde{\chi}_2^0}$ in the compressed-slepton scenario at the FCC-eh.

FIG. 6. Significance shown as a function of the mass difference $\Delta m = m_{\tilde{\ell}} - m_{\tilde{\chi}^\pm_1,\tilde{\chi}_2^0}$ when fixing electroweakino masses, $m_{\tilde{\chi}^\pm_1,\tilde{\chi}_2^0} = 400$ GeV, in the compressed-slepton scenario at the FCC-eh.
FIG. 7. Distributions of BDT response at the FCC-eh for signal $j e^−\tilde{\chi}\tilde{\chi}$ with $m_{\tilde{\chi}_1^±,\tilde{\chi}_1^0} = 250$ GeV (black with filled area) in the decoupled-slepton scenario, and SM background processes of $j e^−\nu\nu$ (red) and $j e^−\ell\nu$ (blue) after applying the pre-selections.

potentially corresponding to 1 $ab^{-1}$. In the last row, significances calculated assuming 5% systematic uncertainties for the backgrounds are also included.

| FCC-eh [1 $ab^{-1}$] | Signal | Background |
|-----------------------|--------|------------|
| $m_{\tilde{\chi}_1^±,\tilde{\chi}_1^0}$ [GeV] | 250 | $j e^−\nu\nu$ | $j e^−\ell\nu$ |
| initial | 909 | $1.08 \times 10^6$ | $7.96 \times 10^6$ |
| Pre-selection | 399 | $3.87 \times 10^5$ | $5.71 \times 10^5$ |
| BDT > 0.251 | 14 | 326 | 357 |
| $\sigma_{\text{stat}+\text{syst}}$ | 0.3 | |

TABLE III. Number of events after selections applied sequentially on the signal $j e^−\tilde{\chi}\tilde{\chi}$ with $m_{\tilde{\chi}_1^±,\tilde{\chi}_1^0} = 250$ GeV in the decoupled-slepton scenario, and for the SM background processes $j e^−\nu\nu$ and $j e^−\ell\nu$. The numbers correspond to an integrated luminosity of 1 $ab^{-1}$ at the FCC-eh with unpolarized electron beam. The significances, calculated including 5% systematic uncertainties on the background, are presented in the last row.

Figure 8 shows the significance as a function of $m_{\tilde{\chi}_1^±,\tilde{\chi}_1^0}$. When considering 0% (5%) systematic uncertainty on the background, the 2-$\sigma$ limits on the $\tilde{\chi}_1^±$ and $\tilde{\chi}_1^0$ masses are 230 (125) GeV for 2.5 $ab^{-1}$ luminosity. Because of the small signal production, the discovery power for the decoupled-slepton scenario is limited at the future $ep$ colliders.

VI. EFFECTS OF BEAM POLARIZATION

The possibility of having a polarized electron beam at the LHeC and FCC-eh colliders could potentially enhance the sensitivity to electroweakinos. A high degree of longitudinal polarization could be envisaged ($|P(e^-)| = 80\%$). When applying an electron beam polarization of -80% (+80%) at the FCC-eh, the production cross sections of SM background processes increase (decrease) by about 55% (20%), compared to the rate in case of unpolarized electron beam. On the other hand, in the case of the compressed-slepton scenario with benchmark $m_{\tilde{\chi}_1^±,\tilde{\chi}_1^0} = 400$ GeV and $m_{\tilde{\chi}} = 435$ GeV, the signal production cross section increases (decreases) by about 80%. In the decoupled-slepton scenario with $m_{\tilde{\chi}_1^±,\tilde{\chi}_1^0} = 250$ GeV, the signal production cross section increases (decreases) by about 40%. The changes in the cross sections are due to the electroweak nature of the interactions involved and the assumptions made: the sleptons considered are superpartners of left-handed electrons, and the gauge bosons and Wino-like electroweakinos couple more to left-handed electrons or sleptons. A negative polarization can be therefore advantageous for such searches of electroweak SUSY particles, whilst a positive polarization might reduce the sensitivity, although a new optimization of the analysis would be needed in this case.

Compared with the unpolarized electron beam with 1 $ab^{-1}$ luminosity, the -80% electron beam polarization increases the significances for the benchmark mass hypothesis in compressed-slepton scenarios by about 40% (15%), from 9 to 13 (3.3 to 3.8) when including 0% (5%) systematic uncertainty on the background. In case of decoupled-slepton scenarios, the -80% electron beam polarization increases the significances by about 30% (10%), from 1.0 to 1.3 (0.32 to 0.35) when including 0% (5%) systematic uncertainty on the background. Hence, thanks to the much larger signal production, our preliminary analysis indicates that the -80% electron beam polarization could lead to a stronger discovery potential for the SUSY electroweak sector especially for the compressed-slepton scenario with small systematic uncertainty. A more accurate simulation and estimate of acceptances and yields in case of polarized electron beams is needed considering several mass hierarchy hypotheses, which is beyond the scope of this study and we leave it for future studies.
The LHC experiments have produced impressive constraints on the masses of the SUSY coloured sector. Because of the low direct production cross sections for neutralinos, charginos and sleptons, the LHC constraints on their masses are limited, particularly in the compressed scenarios where the experimental analysis is challenging, due to the presence of soft momenta decay products. In this article, we have reported a search strategy for the SUSY electroweak sector and its discovery potential at the future electron-proton colliders, LHeC and FCC-eh. Our study shows that the search for the SUSY electroweak sector in the compressed scenarios at the ep colliders could be complementary to the analyses at the pp colliders, mainly due to the cleaner environment and smaller SM background at ep colliders.

We focus on the compressed scenarios where the LSP $\tilde{\chi}_1^0$ is Bino-like, $\tilde{\chi}_1^\pm$ and $\tilde{\chi}_2^0$ are Wino-like with almost degenerate masses, and the mass difference between $\tilde{\chi}_1^\pm$ and $\tilde{\chi}_2^0$ is small. The signal is produced via the process $p e^- \rightarrow j e^- \tilde{\chi} \tilde{\chi}'$, where $\tilde{\chi} = \tilde{\chi}_1^0$, $\tilde{\chi}_1^\pm$ or $\tilde{\chi}_2^0$. LO cross sections are considered for the SUSY signal models, hence results are conservative. The kinematic observables are input to the TMVA package to perform a multivariate analysis at the detector level.

In the compressed-slepton scenario, the case where the left-handed slepton $\tilde{\ell}_L$ and sneutrino $\tilde{\nu}$ are slightly heavier than $\tilde{\chi}_1^\pm$ or $\tilde{\chi}_2^0$ is considered. When fixing the mass difference $\Delta m = m_{\tilde{\ell}} - m_{\tilde{\chi}_1^\pm} = 35$ GeV and ignoring the systematic uncertainty on the background, our analysis indicates that the 2 (5)-$\sigma$ limits on the $\tilde{\chi}_1^\pm$, $\tilde{\chi}_2^0$ mass are 616 (517) GeV for 2.5 ab$^{-1}$ luminosity at the FCC-eh, and 266 (227) GeV for 1 ab$^{-1}$ luminosity at the LHeC, respectively. The effects of varying $\Delta m$ are investigated: fixing $m_{\tilde{\chi}_1^\pm}, m_{\tilde{\chi}_2^0}$ to be 400 GeV, we find that at the FCC-eh the significance is maximal when $\Delta m$ is around 20 GeV.

In the decoupled-slepton scenarios where only $\tilde{\chi}_1^0$, $\tilde{\chi}_1^\pm$ and $\tilde{\chi}_2^0$ are light and other SUSY particles are heavy and decoupled, the 2-$\sigma$ limits obtained on the $\tilde{\chi}_1^\pm$, $\tilde{\chi}_2^0$ mass are 230 GeV for 2.5 ab$^{-1}$ luminosity at the FCC-eh when neglecting the systematic uncertainty on the background. Large systematic uncertainties on the SM background processes can substantially affect the sensitivity, hence good control of experimental and theoretical sources of uncertainties is very important. Finally, it is found that the possibility of having a negatively polarized electron beam ($Pe^- = 80\%$) could potentially extend the sensitivity to electroweakinos by up to 40%.

Overall, since the sensitivity to the electroweak SUSY sector depends on the mass hierarchy of $\tilde{\chi}_1^\pm$, $\tilde{\chi}_1^0$, $\tilde{\chi}_2^0$ and sleptons, and given the difficulty to probe efficiently small $\Delta m$ regions at the current LHC and possibly at the HL-LHC, measurements at ep colliders may prove to offer complementary or additional reaches, in particular for the compressed scenarios.

ACKNOWLEDGMENTS

We thank Oliver Fisher, Satoshi Kawaguchi, Max Klein, Uta Klein, and Peter Kostka for helpful communication. We appreciate comments from members in the LHeC / FCC-eh Higgs and BSM physics study groups. K.W. thanks Christophe Grojean and Cai-dian Li for their supports. G.A. is supported by National Science and Engineering Research Council (Canada). The work of S.I. is partially supported by the MIUR-PRIN project 2015P5SBHT 003 “Search for the Fundamental Laws and Constituents”. K.W. is supported by the Excellent Young Talents Program of the Wuhan University of Technology, the National Natural Science Foundation of China under grant no. 11905162, and the CEPC theory grant (2019–2020) of IHEP, CAS.

Appendix A: Distributions of Input Observables
FIG. 9. Kinematial distributions of some input observables for signal $j e^- \tilde{\chi}$ with $m_{\tilde{\chi}^0_1} = 400$ GeV (black with filled area) in the compressed-slepton scenario, and for the SM background of the $j e^- \nu \nu$ (red) and $j e^- \ell \nu$ (blue) processes after applying the pre-selection cuts at the FCC-eh with an unpolarized electron beam.

FIG. 10. Kinematial distributions of some input observables for signal $j e^- \tilde{\chi}$ with $m_{\tilde{\chi}^0_1} = 250$ GeV (black with filled area) in the compressed-slepton scenario, and for the SM background of the $j e^- \nu \nu$ (red) and $j e^- \ell \nu$ (blue) processes after applying the pre-selection cuts at the LHeC with an unpolarized electron beam.
ground of the area) in the decoupled-slepton scenario, and for the SM back-
larized electron beam.

FIG. 11. Kinematal distributions of some input obervables

[1] CMS, A. M. Sirunyan et al., Searches for physics bey-
ond the standard model with the $M_{T2}$ variable in hadronic final states with and without disappearing tracks in proton-proton collisions at $\sqrt{s} = 13$ TeV, (2019), arXiv:1909.03460, CMS-SUS-19-005, CERN-EP-2019-180.

[2] CMS, A. M. Sirunyan et al., Search for supersymmetry in proton-proton collisions at 13 TeV in final states with jets and missing transverse momentum, JHEP 10, 244 (2019), arXiv:1908.04722, CMS-SUS-19-006, CERN-EP-2019-152.

[3] ATLAS, T. A. collaboration, Search for squarks and gluinos in final states with jets and missing transverse momentum using 139 fb$^{-1}$ of $\sqrt{s} = 13$ TeV pp collision data with the ATLAS detector, (2019), ATLAS-CONF-2019-040.

[4] ATLAS, M. Aaboud et al., Search for electroweak production of supersymmetric states in scenarios with compressed mass spectra at $\sqrt{s} = 13$ TeV with the ATLAS detector, Phys. Rev. D97, 052010 (2018), arXiv:1712.08119, CERN-EP-2017-297.

[5] ATLAS, M. Aaboud et al., Search for electroweak produ-
ction of supersymmetric particles in final states with two or three leptons at $\sqrt{s} = 13$ TeV with the ATLAS detector, Eur. Phys. J. C78, 995 (2018), arXiv:1803.02762, CERN-EP-2017-303.

[6] ATLAS, M. Aaboud et al., Search for chargino-neutralino production using recursive jigsaw reconstruction in final states with two or three charged leptons in proton-proton collisions at $\sqrt{s} = 13$ TeV with the ATLAS detector, Phys. Rev. D98, 092012 (2018), arXiv:1806.02293, CERN-EP-2018-113.

[7] ATLAS, M. Aaboud et al., Search for chargino and neut-
ralino production in final states with a Higgs boson and missing transverse momentum at $\sqrt{s} = 13$ TeV with the ATLAS detector, Phys. Rev. D100, 012006 (2019), arXiv:1812.09432, CERN-EP-2018-306.

[8] CMS, A. M. Sirunyan et al., Search for electroweak produ-
cion of charginos and neutralinos in WH events in proton-proton collisions at $\sqrt{s} = 13$ TeV, JHEP 11, 029 (2017), arXiv:1706.09933, CMS-SUS-16-043, CERN-EP-2017-113.

[9] CMS, A. M. Sirunyan et al., Search for electroweak pro-
duction of charginos and neutralinos in multilepton final states in proton-proton collisions at $\sqrt{s} = 13$ TeV, JHEP 03, 166 (2018), arXiv:1709.05406, CMS-SUS-16-039, CERN-EP-2017-121.

[10] CMS, A. M. Sirunyan et al., Search for supersymmetry with Higgs boson to diphoton decays using the razor variables at $\sqrt{s} = 13$ TeV, Phys. Lett. B779, 166 (2018), arXiv:1709.00384, CMS-SUS-16-045, CERN-EP-2017-158.

[11] CMS, A. M. Sirunyn et al., Search for new pheno-
mena in final states with two opposite-charge, same-
flavor leptons, jets, and missing transverse momentum in

pp collisions at $\sqrt{s} = 13$ TeV, JHEP 03, 076 (2018), arXiv:1709.08908, CMS-SUS-16-034, CERN-EP-2017-170.

[12] CMS, A. M. Sirunyn et al., Search for new physics in

events with two soft oppositely charged leptons and
missing transverse momentum in proton-proton collisions

at $\sqrt{s} = 13$ TeV, Phys. Lett. B782, 440 (2018), arXiv:1801.01846, CERN-EP-2017-336, CMS-SUS-16-048.

[13] CMS, A. M. Sirunyn et al., Combined search for
electroweak production of charginos and neutralinos in

proton-proton collisions at $\sqrt{s} = 13$ TeV, JHEP 03, 160 (2018), arXiv:1801.03957, CMS-SUS-17-004, CERN-EP-2017-283.

[14] CMS, A. M. Sirunyn et al., Search for supersymmetric partners of electrons and muons in proton-proton collisions at $\sqrt{s} = 13$ TeV, Phys. Lett. B790, 140 (2019), arXiv:1806.05264, CMS-SUS-17-009, CERN-EP-2018-132.

[15] CMS, A. M. Sirunyn et al., Search for supersymmetry with a compressed mass spectrum in the vector boson fusion topology with 1-lepton and 0-lepton final states in proton-proton collisions at $\sqrt{s} = 13$ TeV, JHEP 08, 150 (2019), arXiv:1905.13059, CMS-SUS-17-007, CERN-EP-2019-093.

[16] ATLAS, T. A. collaboration, Search for electroweak pro-
duction of charginos and sleptons decaying in final states

with two leptons and missing transverse momentum in

$\sqrt{s} = 13$ TeV pp collisions using the ATLAS detector,
ATLAS, Extrapolation of $E_{\text{T}}^{\text{miss}} + \text{jet}$ search results to an integrated luminosity of 300 fb$^{-1}$ and 3000 fb$^{-1}$, (2018), ATL-PHYS-PUB-2018-043, https://cds.cern.ch/record/2650050.