Wireless Network Coding with Intelligent Reflecting Surfaces

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Abstract—Conventional wireless techniques are becoming inadequate for beyond fifth-generation (5G) networks due to latency and bandwidth considerations. To improve the error performance and throughput of wireless communication systems, we propose physical layer network coding (PNC) in an intelligent reflecting surface (IRS)-assisted environment. We consider an IRS-aided butterfly network, where we propose an algorithm for obtaining the optimal IRS phases. Also, analytic expressions for the bit error rate (BER) are derived. The numerical results demonstrate that the proposed scheme significantly improves the BER performance. For instance, the BER at the relay in the presence of a 32-element IRS is three orders of magnitudes less than that without an IRS.

Index Terms—Intelligent reflecting surfaces; network coding; butterfly networks; performance analysis

I. INTRODUCTION

Conventional wireless communication techniques are becoming inadequate for beyond fifth-generation (5G) networks because they, in general, have excessive network latency and low spectral efficiency [1]. Network coding is a promising solution to increase the throughput of wireless networks [2], [3]. It relies on the ability of the relay (router) to perform more complex operations than just forwarding [4]. One kind of network coding is physical layer network coding (PNC), where the physical broadcast nature of wireless links, which generally causes deleterious interference, is exploited to increase the network throughput [2]–[6]. Yet, higher bandwidth is required to support PNC with higher data rates, which necessitates a move toward the millimeter wave (mm-Wave) band. However, mm-Wave communication suffers from high path loss and is susceptible to blockages. These limitations suggest future sustainable networks, where the propagation channel itself can be controlled.

In this regard, so-called intelligent reflecting surfaces (IRSs) have been demonstrated to overcome some of the issues associated with mm-Waves [7]. An IRS is a flat surface which comprises many small passive elements, each of which can independently introduce phase changes to the incident signals [8]. Thus, unlike traditional relays, it does not need a dedicated energy source or consume any transmit power. An IRS can be easily integrated into walls, ceilings, and building facades [9].

IRSs can enhance communication performance in terms of coverage, energy efficiency, electromagnetic radiation reduction, and wireless localization accuracy [10]–[14]. Also, IRSs can improve the bit error rate (BER) performance of over-air-computation (OAC) techniques [15]–[17]. This is achieved by smartly tuning the IRS phase profile, thereby significantly boosting the received signal power. In a sense, PNC is a kind of OAC as it is based on the linear or nonlinear aggregation of signals by the wireless medium; yet it has remained unstudied in the presence of IRSs.

In this paper, we propose a PNC scheme in an IRS-assisted environment to enhance the error performance and throughput of wireless communication systems, especially in unfavorable channel conditions for mm-Wave communication. As a proof of concept, we focus on the butterfly network, usually adopted as the basic setting in the framework of network coding [5], [18]. In this setting, the relay computes network-coded packets directly from the received signal. To improve BER performance, we optimize the IRS profile. Although, the problem is non-convex, we propose an efficient optimization algorithm based in matrix lifting. Then, we derive the analytic BER of IRS-aided butterfly network to judge error performance. Numerical results verify the significant improvement of BER performance due to the proposed scheme.

For notation, the probability of an event and expectation of a random variable are denoted by $\mathbb{P}\{\cdot\}$ and $\mathbb{E}\left[\cdot\right]$, respectively. Capital bold letters, e.g., $\mathbf{X}$, and small bold letters, e.g., $\mathbf{x}$, denote matrices and vectors, respectively. The notation $\text{diag}(\mathbf{x})$ represents a diagonal matrix with diagonal $\mathbf{x}$, while $\text{tr}(\cdot)$ denotes the matrix trace. The transpose and Hermitian of vectors or matrices are denoted as $(\cdot)^T$ and $(\cdot)^H$. The $l^{th}$ row and column of a matrix $\mathbf{X}$ are denoted by $\mathbf{x}_{(l)}$ and $\mathbf{x}_l$, respectively. The real part of complex number $z$ is denoted by $\Re(z)$. The $\ell_2$-norm of a vector $\mathbf{x}$ is denoted by $||\mathbf{x}||$.

II. SYSTEM MODEL

This paper considers the IRS-aided butterfly network as shown in Fig. 1 where sources $S_1$ and $S_2$ want to deliver their messages to destinations $D_1$ and $D_2$. For simplicity, we assume each source and destination node have a single antenna to transmit and receive, respectively, whereas the relay node is equipped with $N_r = 2$ antennas. To enhance communication performance from $N_s = 2$ sources to relay, we propose deploying an IRS with $M$ reflecting elements, as in Fig. 1.

There are two stages in PNC. In the first stage, $S_1$ and $S_2$ broadcast their data to the relay and to destinations $D_1$ and
where \( D = 2D^{-1} = \begin{bmatrix} 1 & 1 \\ 1 & -1 \end{bmatrix} \) is the sum-difference matrix, and \( \bar{x} \) is
\[
\bar{x} = \begin{bmatrix} x_1 \\ x_2 \end{bmatrix} \triangleq Dx = \begin{bmatrix} x_1 + x_2 \\ x_1 - x_2 \end{bmatrix}.
\]
The vector \( \bar{x} \) can be estimated from \( r \) using a linear operator as
\[ y = Gr, \]
where \( G \in \mathbb{C}^{N_r \times N_r} \) is the beamforming matrix at the relay, designed in Section IV. We consider that the relay can estimate the channel state information (CSI).

III. PROBLEM FORMULATION

In this section, we aim to design the optimal linear operator, i.e., the beamforming matrix \( G \) and the IRS phase profile \( \Theta \) to minimize the mean-squared error (MSE) for the recovery of \( \bar{x} \). In this regard, the problem can be formulated as

\[
\begin{align*}
\text{minimize} & \quad \text{MSE} \triangleq E \left[ \|y(\Theta, G) - \bar{x}\|^2 \right] \\
\text{subject to} & \quad 0 \leq \theta_m \leq 2\pi, \ m \in \{1, 2, \ldots, M\}.
\end{align*}
\]

The MSE between the estimate \( y \) and target parameter \( \bar{x} \) can be computed as
\[
\text{MSE} = \text{tr} \left( \mathbb{E} \{ (Gr - \bar{x}) (r^H G^H - \bar{x}^H) \} \right)
= \text{tr} \left( \mathbb{E} \{ r (r^H G^H - \bar{x}^H) \} + \mathbb{E} \{ \bar{x} \bar{x}^H \} \right)
= \text{tr} \left( G (PHH^H + \sigma^2 I) G^H - 2R \{ GPHD^H \} + 2PI \right).
\]

The joint optimization over the beamforming matrix and IRS profiles in (6) is challenging. In Section IV, we provide an efficient algorithm for the optimization problem.

IV. OPTIMIZATION ALGORITHM

We propose an algorithm that optimizes the IRS phases while fixing the beamforming matrix in (6). In particular, for a fixed \( \Theta \) in (6), the optimization problem is a quadratic unconstrained problem in \( G \) that can be solved in a closed-form as
\[ G = (PHH^H + \sigma^2 I)^{-1} PHH^H, \]
which is the minimum mean square error (MMSE) estimator for \( G \). To optimize the phases of IRS for fixed \( G \), we propose the matrix lifting technique [20]. First, the objective function should be written in terms of \( v \), i.e., MSE can be written as
\[
\text{MSE} \triangleq P \sum_{i=1}^{N_s} \sum_{j=1}^{N_r} \sum_{l=1}^{N_c} \sum_{m=1}^{N_c} s_l^H g_{jl}^i \phi_l^i \left( b^{ij} \right)^H b^{j'i} + 2PN_s
\]
\[ - 2P \Re \left( \sum_{i=1}^{N_s} \sum_{j=1}^{N_r} \sum_{m=1}^{N_c} \sum_{n=1}^{N_c} \sigma_n^2 g_{jl}^i (g_{mj} + (-1)^{i+j} g_{nj}) \right) + \sum_{i=1}^{N_s} \sigma_i^2, \]
where \( b^{ij} = \phi_l^i v + h_{jl}^i \) and \( \phi_l^i = h_{jl}^i \phi_l^i \).
By substituting (9) in (9), we can write the optimization problem (6) for a fixed \( G \) as:

\[
\begin{aligned}
\text{minimize} & \quad \text{MSE} \\
\text{subject to} & \quad |v(m)|^2 = 1, \ m \in \{1, 2, \ldots, M\}. 
\end{aligned}
\] (10a)

The unit modulus constraint induces non-convexity. In this regard, we apply a matrix lifting technique [20]. Now, the problem is tackled with the help of matrix \( V \), where

\[
V = \left[ \begin{array}{c|c} V & \frac{V H}{1} \end{array} \right] = \left[ \begin{array}{c|c} vV & v \\
V H & 1 \end{array} \right].
\] (11)

For \( V \), we have the following constraints: \( \text{rank}(V) \leq 1, \ V \geq 0, \) and \( V(k, k) = 1, \ \forall k \in \{1, 2, \ldots, M+1\} \). Let us rewrite (9) in terms of \( V \) and remove all the terms that do not depend on \( v \) as

\[
\begin{aligned}
\text{MSE} & \propto \sum_{i=1}^{N_g} \sum_{j=1}^{N_r} \sum_{k=1}^{N_l} \left( g_{ij}^* g_j^H \left[ \begin{array}{cccc}
\phi_{ji}^H & \phi_j^H & 0 & 0 \\
\phi_j^H & \phi_{ji}^H & 0 & 0 \\
h_{ji}^* & h_{ji} & 0 & 0 \\
h_{ji} & h_{ji}^* & 0 & 0
\end{array} \right] V - \sum_{i=1}^{N_g} \sum_{j=1}^{N_r} \left( \begin{array}{c}
0 \\
0 \\
0 \\
0
\end{array} \right) \phi_{ji} \left( g_{ij} + (-1)^i g_{ji}^* \phi_{ji}^H \right) \right) \right) \\
& = \text{tr}(AV),
\end{aligned}
\] (12)

where \( A \) is a matrix representing the summation of all the matrices inside the trace function in (13). So, we have the following optimization problem

\[
\begin{aligned}
\text{minimize} & \quad \text{tr}(AV) \\
\text{subject to} & \quad V(k, k) = 1, \ k \in \{1, 2, \ldots, M+1\} \\
& \quad \text{rank}(V) \leq 1.
\end{aligned}
\] (13a)

(13b)

(13c)

The constraint \( \text{rank}(V) \leq 1 \) is non-convex and equivalent to

\[
\text{tr}(V) - \beta_1(V) = 0,
\] (14)

where \( \beta_1(V) \) is the largest singular value of the matrix \( V \). Also, for \( V \geq 0, \) i.e., semidefinite, the left side of (14) is 0 when \( \text{rank}(V) \leq 1 \) is satisfied; otherwise, it is greater than zero. The optimization problem can be written as

\[
\begin{aligned}
\text{minimize} & \quad \text{tr}(AV) + \gamma (\text{tr}(V) - \beta_1(V)) \\
\text{subject to} & \quad V(k, k) = 1, \ k \in \{1, 2, \ldots, M+1\},
\end{aligned}
\] (15a)

(15b)

where \( \gamma \geq 0 \) is a fixed weight. Since \( \beta_1(V) \) and \( \text{tr}(AV) + \gamma \text{tr}(V) \) are convex functions in \( V \), [15] can be represented as a difference-of-convex functions (DC) problem. Concave convex procedure (CCP) can efficiently obtain a local optimal solution for DC problems [21]. In this regard, we linearize \( -\gamma \beta_1(V) \), which induces non-convexity in (15), around a point \( V = V^* \) using the following upper bound [16]

\[
-\gamma \beta_1(V) \leq -\gamma \text{tr} \left( V u_1(V^*) u_1(V^*)^H \right),
\] (16)

where \( u_1(V^*) \) is the eigenvector of the matrix \( V^* \) corresponding to its largest eigenvalue. The equality condition in (16) is satisfied when \( V = V^* \). We get the following convex optimization problem, which can be solved by cvx:

\[
\begin{aligned}
\min_{V \succeq 0} & \quad \text{tr}(AV) + \gamma \left( \text{tr}(V) - \text{tr} \left( V u_1(V^*) u_1(V^*)^H \right) \right) \\
\text{s.t.} & \quad V(k, k) = 1, \ k \in \{1, 2, \ldots, M+1\}.
\end{aligned}
\] (17a)

(17b)

Appropriate choice of the penalty parameter \( \gamma \) in (17) can be found via simple bisection and remains static throughout Alg. 1. An iterative algorithm that alternately optimizes the phases of IRS and beamforming matrix \( G \) is given in Alg. 2.

V. OPTIMAL DETECTOR AND ERROR PERFORMANCE

A. Optimal Detector

The likelihood estimator can be considered to estimate the network coding form, i.e., \( x_0, \) from \( y \). In this regard, the log likelihood ratio (LLR) can be written, ignoring the noise dependencies in \( y_1 \) and \( y_2, \) as

\[
\begin{aligned}
\mathcal{L}(x_0|y_1 y_2) &= \log \left( \frac{P\{y_1 y_2|x_0 = 1\}}{P\{y_1 y_2|x_0 = -1\}} \right) \\
&= \log \left( \frac{P\{y_1|x_1 = 0\} P\{y_2|x_2 = 2\} + P\{y_2|x_2 = -2\}}{P\{y_1|x_1 = 2\} + P\{y_1|x_1 = -2\} P\{y_2|x_2 = 0\}} \right) \\
&= 2 \left( \frac{1}{\sigma^2_1} - \frac{1}{\sigma^2_2} + \frac{\cosh(2y_2/\sigma^2_2)}{\cosh(2y_1/\sigma^2_1)} \right),
\end{aligned}
\] (18)

where \( \sigma^2_1 \triangleq \{GG^H\}_{i,i}, \sigma^2_2 \) is the noise variance on the \( i \)th stream after the linear operator. Let us first define the
estimation of \( x_{\oplus} \) at the relay and \( D_1 \) as \( \hat{x}_{\oplus,r} \) and \( \hat{x}_{\oplus,D_1} \), respectively. The corresponding decision rules are then

\[
\hat{x}_{\oplus,r} = \begin{cases} 
  1 & \text{when } \mathcal{L}(x_{\oplus}|y_1y_2) \geq 0 \\
  -1 & \text{when } \mathcal{L}(x_{\oplus}|y_1y_2) < 0
\end{cases}, \quad (19)
\]

\[
\hat{x}_{\oplus,D_1} = \begin{cases} 
  1 & \text{when } \mathcal{L}^r_{D_1}(\hat{x}_{\oplus,r}|y_{D_1}) \geq 0 \\
  -1 & \text{when } \mathcal{L}^s_{D_1}(\hat{x}_{\oplus,r}|y_{D_1}) < 0
\end{cases}, \quad (20)
\]

where \( \mathcal{L}^r_{D_1} = 2y_{D_1}/\sigma_{D_1}^2 \) is the likelihood detector, and \( y_{D_1} \) is the received signal at \( D_1 \) from relay. After the channel inversion, the variance of the noise at \( D_1 \) is \( \sigma_{D_1}^2 = \sigma^2/\|h_{D_1}\|^2 \). After that, the relay broadcasts \( \hat{x}_{\oplus,r} \) to the destinations. \( D_1 \) receives \( \hat{x}_{\oplus,D_1} \) and \( \hat{x}_1 \), which is estimated similarly to \( \hat{x}_{\oplus,D_1} \) with likelihood detector \( \mathcal{L}^s_{D_1} = 2y_{D_1}/\sigma_{D_1}^2 \), received signal \( y_{D_1} \), and noise variance after channel inversion \( \sigma_{D_1}^2 = \sigma^2/\|h_{D_1}\|^2 \). Then, \( \hat{x}_2 \) is obtained at \( D_1 \) by XORing \( \hat{x}_{\oplus,D_1} \) and \( \hat{x}_1 \). Similarly, \( D_2 \) receives \( \hat{x}_2 \) and \( \hat{x}_{\oplus,D_2} \), and obtains \( \hat{x}_1 \) by XORing the two values.

### B. BER Analysis

Before calculating instantaneous theoretical BER at \( D_1 \), i.e., \( \mathbb{P}_{D_1} \triangleq \mathbb{P}(\hat{x}_2 \neq x_2) \), we can find the instantaneous BERs separately for the links from sources to relay, from \( S_1 \) to \( D_1 \), and from relay to \( D_1 \). Let us define the set \( X \triangleq \{-2, 2\} \), which contains all the values of \( \hat{x}_2 \) and \( \hat{x}_1 \) such that \( x_{\oplus} = 1 \) and \( x_{\oplus} = -1 \), respectively. To obtain \( \hat{x} \) at the relay from \( y_1 \) and \( y_2 \), we use the LLR in (13).

To derive \( \mathbb{P}_{\oplus} \triangleq \mathbb{P}(\hat{x}_{\oplus,r} \neq x_{\oplus}) \) at the relay, we need to further rewrite (13) as

\[
\mathcal{L}(x_{\oplus}|y_1y_2) = \sum_{i=1}^{N_s} (-1)^i \left[ \log \left( \sum_{x_{\oplus} \in X} e^{-\frac{(y_i - x_{\oplus})^2}{2\sigma_i^2}} \right) + \frac{y_i^2}{2\sigma_i^2} \right].
\]

Now using the soft minimum approximation \( \log \left( \sum_{j} \exp(-Z_j) \right) \approx -\min_j(Z_j) \) from (22), we can approximate the LLR in (21) as

\[
\mathcal{L}(x_{\oplus}|y_1y_2) = \sum_{i=1}^{N_s} (-1)^i \left[ -\min_{x_{\oplus} \in X} \left( \frac{(y_i - x_{\oplus})^2}{2\sigma_i^2} \right) + \frac{y_i^2}{2\sigma_i^2} \right]
\]

\[
= \sum_{i=1}^{N_s} (-1)^{i+1} \min_{x_{\oplus} \in X} \left( -2y_i\hat{x}_i + \frac{x_{\oplus}^2}{2\sigma_i^2} \right).
\]

Hence, instantaneous \( \mathbb{P}_{\oplus} \) can be approximated as

\[
\mathbb{P}_{\oplus} \approx \mathbb{P}(x_{\oplus} = 1)\mathbb{P}(\mathcal{L} < 0|x_{\oplus} = 1) + \mathbb{P}(x_{\oplus} = -1)\mathbb{P}(\mathcal{L} \geq 0|x_{\oplus} = -1)
\]

\[
= \frac{1}{2} \left[ Q \left( \frac{-2}{\sigma_2} \right) + Q \left( \frac{-2}{\sigma_1} \right) \right] \left( \frac{\sqrt{1 + \frac{\sigma_2^2}{\sigma_1^2}}}{\sigma_1} \right)
\]

\[
+ Q \left( \frac{2}{\sigma_1} \right) \left( \frac{-3 + \frac{\sigma_2^2}{\sigma_1^2}}{\sigma_2 \sqrt{1 + \frac{\sigma_2^2}{\sigma_1^2}}} \right) + Q \left( \frac{2}{\sigma_2} \right) \left( \frac{-3 + \frac{\sigma_1^2}{\sigma_2^2}}{\sigma_1 \sqrt{1 + \frac{\sigma_1^2}{\sigma_2^2}}} \right),
\]

where \( Q(\cdot) \) is the Q-function [23]. Using the channel inversion precoder and likelihood detectors [23], the BERs at \( D_1 \) for a given channel realization are \( \mathbb{P}_{D_1} \triangleq \mathbb{P}(\hat{x}_1 \neq x_1) \) = \( Q(1/\sigma_{D_1}) \) and \( \mathbb{P}_{D_1} \triangleq \mathbb{P}(\hat{x}_{\oplus,D_1} \neq \hat{x}_{\oplus,r}) \) = \( Q(1/\sigma_{D_1}) \). Now, \( \mathbb{P}_{D_1} \) can be derived as

\[
\mathbb{P}_{D_1} = \mathbb{P}_{D_1}^S \left( 1 - \mathbb{P}_{D_1}^r \right) \left( 1 - \mathbb{P}_{\oplus} \right) + \mathbb{P}_{D_1}^r \mathbb{P}_{D_1}^S \mathbb{P}_{\oplus} + \left( 1 - \mathbb{P}_{D_1}^S \right) \times \mathbb{P}_{D_1}^r \left( 1 - \mathbb{P}_{\oplus} \right) + \left( 1 - \mathbb{P}_{D_1}^S \right) \left( 1 - \mathbb{P}_{\oplus} \right) \mathbb{P}_{\oplus}. \quad (24)
\]

Note that the event \( (\hat{x}_2 \neq x_2) \) at \( D_1 \) occurs when the number of links with error is odd. For example, \( \mathbb{P}_{D_1} \left( 1 - \mathbb{P}_{D_1}^r \right) \left( 1 - \mathbb{P}_{\oplus} \right) \) considers that the estimated value of \( x_1 \) at \( D_1 \) is wrong while \( \hat{x}_{\oplus,r} \) and \( \hat{x}_{\oplus,D_1} \) are correct.

### VI. Simulation Results

In this section, we demonstrate the advantages of using IRS and PNC in terms of the BER. The channel coefficients are generated as standard complex Gaussian random variables, and the signal to noise ratio (SNR) is defined as \( \text{SNR} \triangleq P/\sigma^2 \). In all figures, solid and dashed lines represent theoretical and Monte-Carlo simulation results, respectively.

To evaluate the impact of the IRS phase design, the BER at the relay, \( \mathbb{P}_{\oplus} \), versus SNR is depicted in Fig. 2.
various phase designs, i.e., i) optimal: the phases are designed according to the proposed scheme in Section IV; ii) quantized: the optimal phases are quantized to two levels (0 or π); iii) random: the phases are selected uniformly at random from 0 to 2π. It is clear that the Monte-Carlo simulations coincide with the theoretical results. Also, optimizing the IRS phases can significantly decrease the BER. For a target BER of 10^{-2}, the SNR gain compared to random phases is about 18 dB.

The impact of the number of IRS elements on the BER at the relay in Fig. 3. Two phase profiles are considered (optimal and random) along with the case without IRS. For random phases, P_{D_1} decreases slowly, while the proposed phase design allows the BER to rapidly decrease with M.

In Fig. 4 we evaluate the impact of two network coding schemes (PNC and NNC) and two architectures (with and without IRS) on the BER at the destination node, D_2. We can see that the proposed scheme, i.e., PNC combined with IRS, outperforms the schemes that consider NNC and NNC without IRS. The PNC with random and optimal phases have P_{D_2} = 10^{-2} at SNR = 17.85 dB and SNR = 17.8 dB, respectively. Surprisingly, in contrast to the error experienced at the relay in Fig. 2, the gap between the PNC approaches with different IRS designs is negligible. This is attributed to the fact that the BER for the direct link between S_1 and D_2, P_{D_1}, dominates the effect of P_{D_2} while computing the BER at the relay in Fig. 2. Therefore, future works can consider adding two IRSs to enhance the direct links from the sources to destinations, i.e., S_1 − D_1 and S_2 − D_2.

VII. CONCLUSION

We proposed an IRS-aided PNC to improve the wireless network throughput and BER performance. The main contribution is our novel design with IRS that estimates the XOR value of two symbols over-the-air with optimal IRS phases to minimize the estimation error. Also, we derived analytical expressions for the BER. The numerical results show that jointly optimizing the IRS phases and beamforming matrix at the relay offers better performance in terms of the BER. For instance, the BER at the relay in a 32-element IRS-assisted environment is three orders of magnitudes less than that without IRSs. For a target BER of 10^{-2}, we can achieve around 2 dB performance gain in SNR at destinations compared to naive network coding without IRS. As future research directions, our proposed approach can be implemented and analyzed on more complicated network structures with multiple jointly-optimized IRSs.

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