Theoretical Study of Alkaline-Earth Metal (Be, Mg, and Ca)-Substituted Aluminum Nitride Nanocages With High Stability and Large Nonlinear Optical Responses

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By replacing one Al or N atom of aluminum nitride nanocage Al₁₂N₁₂ with an alkaline-earth metal atom, two series of compounds, namely, M@Al₁₂N₁₁ and M@Al₁₁N₁₂ (M = Be, Mg, and Ca), were constructed and investigated in theory. The substituted effect of alkaline-earth metal on the geometric structure and electronic properties of Al₁₂N₁₂ is studied in detail by density functional theory (DFT) methods. The calculated binding energies, HOMO–LUMO gaps, and VIE values of these compounds reveal that they possess high stability, though the NBO and HOMO analyses show that they are also excess electron compounds. Due to the existence of diffuse excess electrons, these alkaline-earth metal-substituted compounds exhibit larger first hyperpolarizabilities (β₀) than pure Al₁₂N₁₂ nanocage. In particular, these considered compounds exhibit satisfactory infrared (IR) (>1800 nm) and ultraviolet (UV) (< 250 nm) transparency. Therefore, these proposed excess electron compounds with high stability may be regarded as potential candidates for new UV and IR NLO molecules.

Keywords: nonlinear optical response (NLO), excess electron compound, aluminum nitride nanocage, first hyperpolarizabilities, density functional theory

INTRODUCTION

Over the past few decades, the design and synthesis of nonlinear optical (NLO) materials with excellent performance have exerted a tremendous fascination on researchers in consideration of their widespread applications in optics and optoelectronics (Marder Seth et al., 1994; Priyadarshy et al., 1996; Nakano et al., 2002; Zhang et al., 2005; Xiao et al., 2008; Xu et al., 2013). Up to now, abundant strategies have been proposed to acquire high-performance NLO materials of the new type, for instance, designing donor–π-conjugated-bridge-acceptor (D–π-A) models (Kanis et al., 1994), decorating or modifying sp²-hybridized carbon nanomaterials (Bai et al., 2013; Muhammad et al., 2013; Yu et al., 2013; Karamanis et al., 2014; Zhou et al., 2014), synthesizing octupolar molecules (Ja Lee et al., 2003), utilizing a multideck sandwich cluster as the building block (Wang et al., 2015), applying the bond length alternation (BLA) theory (Meyers et al., 1994), enhancing push–pull effects (Liu et al., 2010), and doping metal atoms (Di Bella, 2001; Zhong et al., 2012b; Wu et al., 2014), etc. In particular, Chen et al. (2004) and Li et al. (2004) have revealed that the
introduction of loosely bound excess electrons into a molecule is an effective measure to dramatically enhance its NLO response. Therein, the diffuse excess electron is responsible for improved NLO response. Subsequently, a lot of compounds with dispersed excess electrons, namely, excess electron compounds, are designed in theory, and as expected, they exhibit considerable large NLO responses (Zhong et al., 2015).

In previous studies, it has been found that alkali-metal-doped organic complexants exhibit large first hyperpolarizabilities (Chen et al., 2005; Xu et al., 2007; Wang et al., 2012). In these systems, excess electrons are formed when organic complexants push/pull valence electrons of alkali metal atoms. Therefore, such systems were classified as excess electron compounds, where the alkali metal atom acts as the excess electron source. However, the introduction of active alkali metal atoms reduces stability of these compounds. Therefore, selecting the proper excess electron source to achieve new excess electron compounds will be an efficient way to obtain NLO materials with high stability. To achieve this aim, we have used alkali-earth metal atoms as an excess electron source to design several types of excess electron compounds (He et al., 2017a; He et al., 2017b; He et al., 2019) with large first hyperpolarizabilities and satisfying stability.

On the other word, fullerene-like hollow nanocages with noncarbon have attracted great attention owing to their special optoelectronic properties in recent years (Golberg et al., 1998; Strout, 2000; Fu et al., 2001; Stafström et al., 2001; Bertolus et al., 2004; Wang et al., 2005; Beheshtian et al., 2011; Ahmad Peyghan et al., 2012; Beheshtian et al., 2012c). In particular, Group III–V nitrides are the most promising nanoscale materials in various fields. Therefore, a lot of theoretical and experimental studies have been carried out on the Group III-V fullerene-like nanostructures, especially the most significant AlN nanocages because of their high thermal conductivity and chemical stability (Silaghi-Dumitrescu et al., 1996; Oki et al., 2004; Koi et al., 2005; Yang et al., 2005; Zhang and Zhang, 2005; Zope and Dunlap, 2005; Li et al., 2007; Beheshtian et al., 2012a; Liu et al., 2013; Saeedi et al., 2013). Ab initio calculations revealed that the Al12N12 nanocage is the most stable AlN nanostructure and thereby can be regarded as an ideal inorganic fullerene-like candidate (Wu et al., 2003). Considering the unique structural and electronic structure of this cage, it has been used as an excellent starting material to design NLO molecules. For instance, two inorganic electrides, M@Al12N12 (M = Li, Na, and K) (Niu et al., 2014) and M2O@Al12N12 (M = Li, Na, and K) (Sun et al., 2016), were achieved by doping alkali metal atoms and superalkali clusters on the Al12N12 nanocage, while the M@Al12N11 and M@Al11N12 compounds were designed by substituting one atom of Al12N12 with an alkali-metal atom (Maria et al., 2016). All these Al12N12-based excess electron compounds exhibit considerably high NLO responses.

In order to enhance the NLO responses and stability of such Al12N12-based compounds, two series of inorganic compounds, M@Al12N11 and M@Al11N12 (M = Be, Mg, and Ca), were obtained by substituting Al or N atom in the Al12N12 with alkaline-earth metal in the current work. We mainly focus on the following issues: 1) Can loosely bound excess electrons that can dramatically enhance molecular NLO response be generated in these proposed inorganic compounds with alkaline-earth substituted? 2) Do these novel compounds possess larger stability and first hyperpolarizability (β0) than those of previously reported alkali-metal-substituted systems M@Al12N11 and M@Al11N12 (M = Li, Na, and K)? Our results revealed that these inorganic compounds M@Al12N11 and M@Al11N12 (M = Be, Mg, and Ca) indeed contain diffuse excess electrons and thus exhibit larger β0 values than alkali-metal-substituted systems. In particular, These excess electron compounds exhibit excellent infrared (IR) (> 1800 nm) and ultraviolet (UV) (∼ 250 nm) transparency for their potential applications with modern laser frequency conversion technology and optical parameter oscillator processes (Zhang et al., 2009; Luo et al., 2014).

**COMPUTATIONAL DETAILS**

The geometric structures with all real frequencies are obtained by using a combination of Becke’s hybrid 3-parameter exchange functional (Becke, 1993a) and Lee–Yang–Parr’s correlation function (Lee et al., 1988) (B3LYP). In a previous study, the Pople-type (Bilbrey et al., 2013) basis set 6-31+G(d) was selected because it has been proved to be reliable for the geometry optimization of similar systems (Niu et al., 2014). Natural bond orbital (NBO) analyses, vertical ionization energies (VIE), and binding energy (E_b) calculations were also performed at the B3LYP/6-31+G(d) level. The binding energy of the alkaline-earth metal atom M was calculated using the counterpoise procedure (Alkorta and Elguero, 1999) and is defined as follows: For M@Al12N11,

\[
E_b = (E_{Al12N11} + E_M) - E_{M@Al12N11}
\]  

For M@Al12N11,

\[
E_b = (E_{Al12N12} + E_M) - E_{M@Al12N12}
\]

The VIE is the energy difference between neutral molecule and cation systems at the neutral optimization geometry (Wang et al., 2012; Bai et al., 2013; Sun et al., 2015; He et al., 2019). Polarizability and first hyperpolarizability calculations are carried out on long-range correlated methods CAM-B3LYP (Tawada et al., 2004; Yanai et al., 2004) and BHandHLYP (Becke, 1993b) in conjunction with the 6-31+G(d) basis set. As all the systems are in the doublet states, values of spin eigenvalue \(S^2\) involved in the structural optimization and NLO computations are in the range of 0.760–0.789, which shows an error range of 1.3%–4.9%, indicating that the spin contamination is negligible in the current calculations.

The static polarizability \(\alpha_0\) and the first hyperpolarizability \(\beta_0\) are defined as follows:

\[
\alpha_0 = \frac{1}{3} \left( \alpha_{xx} + \alpha_{yy} + \alpha_{zz} \right),
\]

\[
\beta_0 = \sqrt{\beta_{xx}^2 + \beta_{yy}^2 + \beta_{zz}^2},
\]

where \(\beta_{ii}, \beta_{ij}, \beta_{ij}, \beta_{ik}\), and \(i, j, k = x, y, z\).
For electronic transition properties, the transition energy $\Delta E$, oscillator strength $f_0$, and the difference of dipole moment $\Delta \mu$ between the ground and the crucial excited state are estimated by the time-dependent density functional theory, TD-CAM-B3LYP, with the 6-31+G(d) basis set. Simultaneously, ultraviolet-visible-infrared (UV-VIS-IR) absorption spectra of all the systems were also obtained at the same level. All the UV-VIS-IR spectra were reflected with Gaussian curves under a full-width at half-maximum (FWHM) of 0.10 eV.

All of the calculations were carried out by using the Gaussian 16 program package (Frisch et al., 2016). Molecular configurations and molecular orbital (MO) plots were generated with the GaussView program (Dennington et al., 2016).

RESULTS AND DISCUSSION

First, the isolated aluminum nitride nanocage Al$_{12}$N$_{12}$ was optimized, and its structure is shown in Figure 1. In this study, the pure Al$_{12}$N$_{12}$ nanocage is found to be a T$_h$-symmetric fullerene-like cage consisting of six 4-membered rings and eight 6-membered rings, in which the Al–N bond lengths are 1.794 and 1.858 Å, respectively, in consistent with earlier reports (Beheshtian et al., 2012a; Beheshtian et al., 2012b; Niu et al., 2014). Then, the initial geometry structures of M@Al$_{12}$N$_{11}$ and M@Al$_{11}$N$_{12}$ (M = Be, Mg, and Ca) were constructed by replacing one atom (Al or N) in the Al$_{12}$N$_{12}$ nanocage with an alkaline-earth metal atom M. In the M@Al$_{12}$N$_{11}$ series, one alkaline-earth metal atom is substituted for one nitrogen atom, whereas one aluminum atom is replaced with one alkaline-earth metal atom M. In the M@Al$_{11}$N$_{12}$ series, one alkaline-earth metal atom is substituted for one nitrogen atom, whereas one aluminum atom is replaced with one alkaline-earth metal atom M. After optimization, six equilibrium conformations of M@Al$_{12}$N$_{11}$ and M@Al$_{11}$N$_{12}$ have been obtained and are shown in Figure 1. The selected geometrical parameters, VIE values, and HOMO–LUMO gap values of these resulting compounds as well as the binding energies and NBO charges of alkaline-earth metal atoms in them are listed in Table 1.

As shown in Table 1, when one nitrogen or aluminum atom is replaced, the original Al-N bond is elongated. That is to say, the bond lengths of M–Al and M–N in the displaced systems are longer than those of the original Al-N in the pure Al$_{12}$N$_{12}$ nanocage. Nevertheless, the Be-N bond is a special case in Be@Al$_{11}$N$_{12}$. The Be-N bond in the Be@Al$_{11}$N$_{12}$ decreases by ca. 0.175 Å as compared with the Al-N bond in the isolated Al$_{12}$N$_{12}$ nanocage, which may be attributed to the fact that the nitrogen atom possesses larger electronegativity and the Be atom has smaller atomic radii. It is also found that the bond lengths of M–Al and M–N show a monotonous increase with the increasing atomic number of M. In addition, the M–Al bond length of M@Al$_{12}$N$_{11}$ series exhibits a larger increment than the M-N bond length of M@Al$_{12}$N$_{11}$.
length of the M@Al11N12 series as compared with the Al-N bond length of pure Al12N12 nanocage.

Figure 2 displays HOMOs of Al12N12 nanocage, M@Al12N11, and M@Al11N12 (M = Be, Mg, and Ca). It can be seen that the HOMO of a pure Al12N12 nanocage consists of p atomic orbitals of N atoms. Differently, all the HOMOs of M@Al12N11 and M@Al11N12 systems possess diffuse excess electrons, reflecting the unique electric characteristics of these studied compounds. Therefore, these proposed M@Al12N11 and M@Al11N12 (M = Be, Mg, and Ca) systems can be regarded as a new type of inorganic excess electron compounds. Interestingly, it is found that these systems exhibit almost the same HOMOs.

NBO analysis was carried out to analyze charge transfer in nanocages and electronic structures of these systems. The computed NBO charges on alkaline-earth metal atoms in these studied compounds are given in Table 1. From Table 1, it can be seen that the NBO charges of alkaline-earth metal atoms in M@Al11N12 (M = Be, Mg, and Ca) are in the range of (1.101–1.798) |e|, which is much larger than the charges (0.496–0.788) |e| (Maria et al., 2016) on alkali metal atoms in M@Al11N12 (M = Li, Na, and K) and the charges of (0.32-0.60) |e| (Ullah et al., 2020) on alkaline-earth metal atoms in AEM@Al12N12 (M = Be, Mg, and Ca), indicating that more charges are transferred from alkaline-earth metal atoms to the nanocages in these compounds. In addition, it is also found that the charges on M atoms in the M@Al11N12 series are more electropositive than those of the M@Al12N11 series, which may be attributed to the fact that the electronegativity of the nitrogen atom is larger than that of the aluminum atom. When an alkaline-earth metal atom is substituted for an Al atom or N atom, the nitrogen atom has a stronger ability to absorb electrons than the Al atom. Therefore, introducing M atoms in the M@Al11N12 series loses more electrons and displays more electropositivity. Additionally, it is found that the charges on M atoms increase along with the increasing M atomic number in both series because of the increasing electropositivity of M. Moreover, the NBO analysis also reveals that the alkaline-earth metal atoms can serve as the source of diffuse excess electrons for these excess electron compounds.

It is known that the stability of molecules is of great significance for their synthesis in the laboratory and further application in practice. Moreover, the kinetic stability, chemical reactivity, and optical polarizability of any molecule can be described from the energy gap between the highest occupied molecular orbital (HOMO) and the lowest unoccupied molecular orbital (LUMO). HOMO–LUMO gaps of all the studied excess electron compounds are calculated and are summarized in Table 1. As can be seen from Table 1, pure Al12N12 has a large band gap of 3.84 eV, which is a barrier in the way of its applications in electronic devices. As compared with Al12N12, a crucial decrease in the HOMO–LUMO gap was noticed for all replaced systems. That is to say, the HOMO–LUMO gaps of M@Al12N11 and M@Al11N12 are reduced to (1.19–2.32) eV. Even so, the gap values of M@Al12N11 (M = Be, Mg, and Ca) compounds are much larger than those (1.39–1.78) eV (Maria et al., 2016) of M@Al12N11 (M = Li, Na, and K) compounds, comparable to that (1.57 eV) (Wang et al., 1999) of the kinetically stable C60, and those (1.59–3.79) eV (Ullah et al., 2020) of AEM@Al12N12 (M = Be, Mg, and Ca), suggesting the large chemical stability of the studied M@Al12N11 (M = Be, Mg, and Ca) species. From Figure 3, it is also found that the gap values decrease along with the decreasing M atomic number for the M@Al12N11 series, whereas they are hardly equal for the M@Al11N12 series.

Furthermore, the large electronic stability of these excess electron compounds can also be characterized by their higher vertical ionized energies (VIEs) of (5.93–8.95) eV, which are slightly higher than the reported values of inorganic and organic excess electron compounds (Chen et al., 2005; Zhong et al., 2012a; He et al., 2017a; He et al., 2017b; Ullah et al., 2020), indicating that these proposed nanocage compounds exhibit high electronic stability. Figure 3 demonstrates the alkaline-earth metal
atomic number effect on VIE values, namely, the larger the atomic number, the smaller the VIE value.

Additionally, the binding energies ($E_b$) of these designed M@Al$_{12}$N$_{11}$ and M@Al$_{11}$N$_{12}$ compounds are also calculated and given in **Table 1**. The $E_b$ values are defined as the negative of the intramolecular interaction energies between the alkaline-earth metal M and the remaining Al$_{12}$N$_{11}$ or Al$_{11}$N$_{12}$ moieties. Thus, the larger the $E_b$ value is, the stronger the interaction between two subunits. From **Table 1**, it can be seen that all the proposed excess electron compounds exhibit much larger $E_b$ values of (33.0-244.0) kcal/mol than those (31-89 kcal/mol) (Maria et al., 2016) of previously reported alkali-metal substituted compounds, indicating that alkaline-earth metal atoms are more tightly bound to the remaining Al$_{12}$N$_{11}$ or Al$_{11}$N$_{12}$ units than the alkali metal atoms in M@Al$_{12}$N$_{11}$ and M@Al$_{11}$N$_{12}$ (M = Li, Na, and K). More importantly, the M@Al$_{11}$N$_{12}$ (M = Be, Mg, and Ca) series exhibit extremely large $E_b$ values up to (173-244) kcal/mol, which are far more than those of (64-89) kcal/mol for M@Al$_{12}$N$_{11}$ (M = Li, Na, and K) (Maria et al., 2016). Thus, as compared with alkali metal atoms, the introduction of alkaline-earth metal atoms into the Al$_{12}$N$_{12}$ nanocage can produce more stable species with excess electrons. In addition, the $E_b$ values of proposed alkaline-earth metal substituted excess electron compounds are also comparable to those (59-106) kcal/mol of small clusters with alkaline-earth metal atoms (Srivastava et al., 2018).

To evaluate nonlinear optical response, the dipole moments ($\mu_0$), polarizabilities ($\alpha_0$), and first hyperpolarizabilities ($\beta_0$) of pure Al$_{12}$N$_{12}$ and the proposed M@Al$_{12}$N$_{11}$ and M@Al$_{11}$N$_{12}$ (M = Be, Mg, and Ca) series were calculated and are summarized in **Table 2**. To better visualize the results, the dependences of the polarizability ($\alpha_0$) and first hyperpolarizability ($\beta_0$) values on the alkaline-earth metal atomic number are exhibited in **Figure 4**. Our results revealed that the $\alpha_0$ (286 au) of the Al$_{12}$N$_{12}$ nanocage is increased to 319-410 au for replaced compounds, indicating that the substitution of alkaline-earth metal atoms virtually affects the $\alpha_0$ value of the Al$_{12}$N$_{12}$ molecule. As shown in **Table 2** and **Figure 4**, the $\alpha_0$ changes in the order of 331 au (Be) < 369 au (Mg) < 410 au (Ca).
< 410 au (Ca) in the M@Al12N11 series and similarly, varies in the order of 312 au (Be) < 326au (Mg) < 345au (Ca) in the M@ Al11N12 series. In short, α0 increases along with the increasing M atomic number. Also, it is observed that the M@Al12N11 exhibits a relatively larger α0 value than the corresponding M@Al11N12, indicating that the excess electrons in the HOMOs of the former are more diffuse than the latter because static polarizability is sensitive to electronic delocalization.

Due to the pure Al12N12 nanocage being centrosymmetric, its β0 values are zero. Thus, different from α0, the substitution of M for Al or N atom in Al12N12 brings a prominent improvement of first hyperpolarizability (β0) of the Al12N12 nanocage, which is because that M-substitution not only destroys the centrosymmetry of Al12N12 but also makes two kinds of replaced systems possessing the dispersed excess electrons. Two different long-range corrected methods were used to calculate the hyperpolarizability β0 values, which have been listed in Table 2. Figure 4 manifests the first hyperpolarizability at CAM-B3LYP for M@Al12N11 and M@ Al11N12 follows the same trend as for BHandHLYP. However, the calculated values at CAM-B3LYP are slightly lower than BHandHLYP.

Additionally, it can be distinctly seen from Table 2 and Figure 4 that the β0 values of Ca-substitution compounds are greatly larger than those of Be-substitution and Mg-substitution compounds, signifying an evident effect of the M atomic number on the NLO responses of M@Al12N11 and M@Al11N12. To be specific, the varying order for β0 is 861au (Be) < 1979au (Mg) < 6140au (Ca) in the M@Al12N11 series, which is consistent with the change sequence of α0 values. That is, the compounds with higher polarizabilities also present relatively higher NLO responses because of the more diffuse excess electrons in them. The comparison of β0 values between our proposed excess electron compounds and previously reported alkali-metal substituted compounds is meaningful. In the M@Al12N11 series, it can be seen that reported alkali-metal substituted compounds exhibit much larger β0 values of (2,500-9,100) au (in CAM-B3LYP/6-311 + g* level) (Maria et al., 2016) than those (861-6,140) au of our proposed alkaline-earth metal substituted excess electron compounds. However, the resultant comparison of β0 values is inverse in the M@Al11N12 series, namely, β0 values (1,628–3,687) au of alkaline-earth metal-substituted compounds are larger than those (420–770) kcal/mol of alkali-metal-substituted compounds. Thus, when a N atom is substituted by alkaline-earth metal atoms in an Al12N12 nanocage, excess electron compounds M@Al11N12 (M = Be, Mg, and Ca) can exhibit larger NLO responses than M@Al11N12 (M = Li, Na, and K).

For intensive discernment of this significant increase in first hyperpolarizability due to substitution of alkaline-earth metal in the Al12N12 nanocage, let us consider the simplest two-level model (Maroulis, 1996; Xu et al., 2009), which is derived from the sum-over states method:

$$\beta_0 = \frac{\Delta\mu f_0}{\Delta E^3},$$

(5)

where involved ΔE, f0, and Δμ are the transition energy, oscillator strength, and difference of the dipole moment between the ground state and the crucial excited state, respectively. The expression distinctly displays that β0 is inversely proportional to the third power of ΔE. Therefore, crucial transition energy plays an important role in the evaluation of β0. In the current work, the TD-CAM-B3LYP calculations are performed to obtain the dominated excited states of these studied compounds. The crucial transitions and the corresponding ΔE, f0, and Δμ values are presented in Table 2 and Figure 5, respectively. It is noted that the electrons involved in the crucial excited states of these considered species primarily come from their HOMO, HOMO-1, and HOMO-2 orbitals. Meanwhile, from Figure 5, it can be seen that crucial transitions make the electrons more diffuse, which may lead to the large β0.

Moreover, compared to the large ΔE value (4.759 eV) in pure Al12N12, the M@Al12N11 and M@Al11N12 compounds exhibit much smaller ΔE values of (0.77-3.32) eV, which are comparable to those of (1.295–1.982) eV for the alkali metal-based electrodes, including Li@(calix [4]pyrrole) (Chen et al., 2005), Li+,H-(CF2-CH2)n-H (n = 1, 2) (Xu et al., 2007), H4C4N2···N3 (Ma et al., 2008), and Li@ B10H14 (Muhammad et al., 2009), and far less than (4.6–6.7) eV of M@Al12N11 and M@Al11N12 (M = Li, Na, and K) (Maria et al., 2016), as well as (1.80–4.76) eV of AEM@Al12N12 (Ullah et al., 2020). Hence, these small ΔE values bring forth the large β0 values of these proposed alkaline-earth metal-based excess electron compounds.
It is well-known that the main applications for NLO materials are in doubling frequency and second harmonic generation (SHG). Accordingly, the superior NLO materials not only need large NLO response but also must be transparent under the applied laser region. Therefore, the ultraviolet-visible–infrared (UV-VIS-NIR) absorption spectra of these M@Al\textsubscript{12}N\textsubscript{11} and M@Al\textsubscript{11}N\textsubscript{12} compounds are gained and shown in Figure 6. From Figure 6A, it can be seen that the main absorption region of M@Al\textsubscript{12}N\textsubscript{11} compounds is from 300 to 500 nm. The absorption of these compounds in the infrared spectral region is weak, especially for Be@Al\textsubscript{12}N\textsubscript{11}, there is no absorption in the visible region of (510–780) nm and the infrared spectral region, which suggests that Be@Al\textsubscript{12}N\textsubscript{11} has satisfying transparency in both the visible region of (510–780) nm and infrared spectral region. In addition, Figure 6B shows that the M@Al\textsubscript{11}N\textsubscript{12} series have an infrared (IR) transparent region at wavelength >1800 nm. Thus, it is hoped that these six excess electron compounds could be used as new IR NLO materials. Simultaneously, it is observed that they also have an ultraviolet (UV) transparent region at wavelength < 250 nm. Then, they may be taken as a new candidate for UV NLO materials.
CONCLUSIONS

Using the density functional theory (DFT), two new series of excess electron compounds, i.e., M@Al$_2$N$_{11}$/ and M@Al$_{11}$N$_{12}$ (M = Be, Mg, and Ca), have been obtained and studied theoretically in this work. The substituted effect of alkaline-earth metal on the geometric structures and electronic properties of aluminum nitride (Al$_2$N$_{12}$) nanocage has been investigated in detail. Binding energy calculations display that these proposed compounds, particularly the Al-replaced nanocages have high structural stability. In addition, the substitution of alkaline-earth metal for Al and N in Al$_2$N$_{12}$ significantly reduces its HOMO–LUMO gap and VIE value, which may bring forth large optical polarizability. More importantly, these studied compounds contain diffuse excess electrons and thus show high NLO responses. Particularly, our results reveal that all these considered compounds show satisfying infrared (IR) transparent region (>1800 nm) and ultraviolet (UV) region (<250 nm). Thus, we hope that this study could not only provide new candidates of potential NLO molecules but also promote future applications of Al-N fullerene-like nanocages in the field of nonlinear optics.

REFERENCES

Ahmadi Peyghan, A., Pashangpour, M., Bagheri, Z., and Kamfiroozi, M. (2012). Energetic, Structural, and Electronic Properties of Hydrogenated Al$_2$P$_{12}$ Nanocluster. Phys. E Low-dimensional Syst. Nanostructures 44 (7), 1436–1440. doi:10.1016/j.pse.2012.03.007

Alkorta, I., and Elguero, J. (1999). Theoretical Study of Strong Hydrogen Bonds between Neutral Molecules: The Case of Amine Oxides and Phosphine Oxides as Hydrogen Bond Acceptors. J. Phys. Chem. A 103 (2), 272–279. doi:10.1021/jp982644m

Bai, Y., Zhou, Z.-J., Wang, J.-J., Li, Y., Wu, D., Chen, W., et al. (2013). New Acceptor-Donor Strategy for Enhancing NLO Response with Long-Range Excess Electron Transfer from the NH$_2$M/M$_3$O Donor (M = Li, Na, K) to the inside the Electron Hole Cage C20F19 Acceptor through the Unusual π Chain Bridge (CH$_3$)$_2$. J. Phys. Chem. A 117 (13), 2835–2843. doi:10.1021/jp3120594

Becke, A. D. (1993b). A New Mixing of Hartree-Fock and Local Density-functional Theories. J. Chem. Phys. 98 (2), 1372–1377. doi:10.1063/1.464304

Becke, A. D. (1993a). Density-functional Thermochemistry. III. The Role of Exact Exchange. J. Chem. Phys. 98 (7), 5648–5652. doi:10.1063/1.464913

Beheshitian, J., Bagheri, Z., Kamfiroozi, M., and Ahmadi, A. (2012a). A Comparative Study on the B$_{12}$N$_{12}$, Al$_{12}$N$_{12}$, B$_{12}$P$_{12}$, and Al$_{12}$P$_{12}$ Fullerene-like Cages. J. Mol. Model. 18 (6), 2653–2658. doi:10.1007/s00894-011-1286-y

Beheshitian, J., Bagheri, Z., Kamfiroozi, M., and Ahmadi, A. (2011). Toxic CO Detection by B$_{12}$N$_{12}$ Nanocluster. Microelectron. J. 42 (12), 1400–1403. doi:10.1016/j.mejo.2010.10.010

Beheshitian, J., Peyghan, A. A., Bagheri, Z., and Kamfiroozi, M. (2012c). Interaction of Small Molecules (NO, H$_2$, N$_2$, and CH$_4$) with BN Nanocluster Surface. Struct. Chem. 23 (5), 1567–1572. doi:10.1007/s11224-012-9970-9

Beheshitian, J., Peyghan, A. A., and Bagheri, Z. (2012b). Selective Function of Al$_2$N$_{12}$ Nano-Cage towards NO and CO Molecules. Comput. Mater. Sci. 62, 71–74. doi:10.1016/j.commatsci.2012.05.041

Bertolus, M., Finocchi, F., and Millié, P. (2004). Investigating Bonding in Small Silicon-Carbon Clusters: Exploration of the Potential Energy Surfaces of Si$_3$C$_4$, Si$_6$C$_6$, and Si$_8$C$_8$ Using Ab Initio Molecular Dynamics. J. Chem. Phys. 120 (9), 4333–4343. doi:10.1063/1.1636717

DATA AVAILABILITY STATEMENT

The raw data supporting the conclusion of this article will be made available by the authors, without undue reservation.

AUTHOR CONTRIBUTIONS

All authors listed have made a substantial, direct, and intellectual contribution to the work and approved it for publication.

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Xiao, D., Bulat, F. A., Yang, W., and Beratan, D. N. (2008). A Donor–Nanotube Paradigm for Nonlinear Optical Materials. *Nano Lett.* 8 (9), 2814–2818. doi:10.1021/nl801388x

Xu, H.-L., Li, Z.-R., Wu, D., Ma, F., Li, Z.-J., and Gu, F. L. (2009). Lithiation and Li-Doped Effects of [5]Cyclacene on the Static First Hyperpolarizability. *J. Phys. Chem. C* 113 (12), 4984–4986. doi:10.1021/jp808684w

Xu, H.-L., Li, Z.-R., Wu, D., Wang, B.-Q., Li, Y., Gu, F. L., et al. (2007). Structures and Large NLO Responses of New Electrides: Li-Doped Fluorocarbon Chain. *J. Am. Chem. Soc.* 129 (10), 2967–2970. doi:10.1021/ja068038k

Xu, X., Hu, C.-L., Kong, F., Zhang, J.-H., Mao, J.-G., and Sun, J. (2013). Cs2GeB4O9: A New Second-Order Nonlinear-Optical Crystal. *Inorg. Chem.* 52 (10), 5831–5837. doi:10.1021/ic302774h

Yanai, T., Tew, D. P., and Handy, N. C. (2004). A New Hybrid Exchange-Correlation Functional Using the Coulomb-Attenuating Method (CAM-B3lyp). *Chem. Phys. Lett.* 393 (1), 51–57. doi:10.1016/j.cplett.2004.06.011

Yang, Z., Shi, L., Chen, L., Gu, Y., Cai, P., Zhao, A., et al. (2005). Synthesis, Characterization and Properties of Novel BN Nanocages from a Single-Source Precursor. *Chem. Phys. Lett.* 405 (1), 229–233. doi:10.1016/j.cplett.2005.02.041

Yu, G., Zhao, X., Niu, M., Huang, X., Zhang, H., and Chen, W. (2013). Constructing a Mixed π-conjugated Bridge: a Simple and Effective Approach to Realize a Large First Hyperpolarizability in Carbon Nanotube-Based Systems. *J. Mat. Chem.* C 1 (24), 3833–3841. doi:10.1039/c3tc00022b

Zhang, D., and Zhang, R. Q. (2005). Geometrical Structures and Electronic Properties of AlN Fullerenes: A Comparative Theoretical Study of AlN Fullerenes with BN and C Fullerenes. *J. Mat. Chem.* 15 (29), 3034–3038. doi:10.1039/B503724G

Zhang, Q., Chung, I., Jang, J. I., Ketterson, J. B., and Kanatzidis, M. G. (2009). Chalcogenide Chemistry in Ionic Liquids: Nonlinear Optical Wave-Mixing Properties of the Double-Cubane Compound [SB7S8Br5][AlCl4]2. *J. Am. Chem. Soc.* 131 (29), 9896–9897. doi:10.1021/ja903881m

Zhang, T.-G., Zhao, Y., Asselberghs, I., Persoons, A., Clays, K., and Therien, M. J. (2005). Design, Synthesis, Linear, and Nonlinear Optical Properties of Conjugated (Porphinato)Zinc(II)-Based Donor–Acceptor Chromophores Featuring Nitrothiophenyl and Nitrooligothiophenyl Electron-Acceptor Moieties. *J. Am. Chem. Soc.* 127 (27), 9710–9720. doi:10.1021/ja0402553

Zhong, R.-L., Xu, H.-L., Li, Z.-R., and Su, Z.-M. (2015). Role of Excess Electrons in Nonlinear Optical Response. *J. Phys. Chem. Lett.* 6 (4), 612–619. doi:10.1021/acs.jpclett.5b00258

Zhong, R.-L., Xu, H.-L., Muhammad, S., Zhang, J., and Su, Z.-M. (2012a). The Stability and Nonlinear Optical Properties: Encapsulation of an Excess Electron Compound LiCN·Li within Boron Nitride Nanotubes. *J. Mat. Chem.* 22 (5), 2196–2202. doi:10.1039/C1JM14358A

Zhong, R.-L., Xu, H.-L., Sun, S.-L., Qiu, Y.-Q., and Su, Z.-M. (2012b). The Excess Electron in a Boron Nitride Nanotube: Pyramidal NBO Charge Distribution and Remarkable First Hyperpolarizability. *Chem. Eur. J.* 18 (36), 11350–11355. doi:10.1002/chem.201201570

Zhou, Z.-J., Yu, G.-T., Ma, F., Huang, X.-R., Wu, Z.-J., and Li, Z.-R. (2014). Theoretical Investigation on Nonlinear Optical Properties of Carbon Nanotubes with Stone-Wales Defect Rings. *J. Mat. Chem. C* 2 (2), 306–311. doi:10.1039/c3tc31904k

Zope, R. R., and Dunlap, B. I. (2005). Electronic Structure of Fullerenelike Cages and Finite Nanotubes of Aluminum Nitride. *Phys. Rev. B* 72 (4), 045439. doi:10.1103/PhysRevB.72.045439

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