Medium Modification of the Proton Form Factor

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Abstract. I argue that the double ratio of proton-recoil polarization-transfer coefficients, \( P'_e \) and \( P'_\mu \), of the quasielastic \(^4\text{He}(e, e'p)\) reaction with respect to the elastic \(^1\text{H}(e, e'p)\) reaction is sensitive to possible medium modifications of the proton form factor in \(^4\text{He}\). Recent measurements at both Mainz and Jefferson Lab of this double ratio at four-momentum transfers squared between between 0.4 (GeV/c)^2 and 2.6 (GeV/c)^2 are discussed. I show that the data challenge state-of-the-art conventional meson-nucleon calculations, as these are unable to describe the results. The data hint at the need to include medium modifications of the proton form factor, as predicted by a quark-meson-coupling model, in the calculations. A recently approved follow-up experiment at a \( Q^2 \) of 0.8 (GeV/c)^2 and 1.3 (GeV/c)^2 with unprecedented precision will provide one of the most stringent tests of the applicability of various calculations.

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1 Introduction

The standard nuclear-physics model describes nuclei as clusters of protons and neutrons held together by a strong force mediated by meson exchange. The success of the nuclear shell model demonstrates that this approximation has been highly effective. A recent example is the very good description of the differential cross section and left-right asymmetry in the \(^{16}\text{O}(e, e'p)\) reaction \(^{[4]}\) with a fully relativistic distorted-wave impulse approximation (RDWIA).

However, protons and neutrons are not the fundamental entities of the underlying theory, quantum chromodynamics. At nuclear densities of about 0.17 nucleons/fm\(^3\), nucleon wave functions have significant overlap. In the chiral limit, one expects nucleons to lose their identity altogether and nuclei to make a transition to a quark-gluon plasma. For that reason, one may expect that, for some observables, the free-nucleon approximation is a highly uneconomical approach. The use of medium-modified nucleons as quasiparticles might be a better choice. To demonstrate that the interpretation of the experimental data is more efficient in terms of medium modifications of nucleon form factors, it is required to have excellent control of the inherent many-body effects, such as meson-exchange currents (MEC) and isobar configurations (IC). In addition, when probing nuclear structure, one has to deal with final-state interactions (FSI).

In unpolarized \( A(e, e'p) \) experiments involving light- and medium-mass nuclei, deviations were observed in the longitudinal/transverse character of the nuclear response compared with the free-proton case \(^{[2,3]}\). Below the two-nucleon-emission threshold, these deviations were originally interpreted as changes in the nucleon form factors within the nuclear medium. However, strong-interaction effects on the ejected proton (final-state interactions) later also succeeded in explaining the observed effect \(^{[5]}\). Still, tantalizing hints of medium effects remain for unpolarized longitudinal/transverse separations in the \(^4\text{He}(e, e'p)\) reaction \(^{[6]}\).

A reaction which is believed to have minimal sensitivity to reaction-mechanism effects is polarization transfer in quasielastic nucleon knockout (see, e.g., \(^{[8]}\)). The polarization-transfer observables are sensitive to the properties of the nucleon in the nuclear medium, including possible modification of the nucleon form factor and/or spinor. This can be seen from free electron-nucleon scattering, where the ratio of the electric to magnetic Sachs form factors, \( G_E \) and \( G_M \), is given by \(^{[9]}\):

\[
\frac{G_E}{G_M} = -\frac{P'_e}{P'_\mu} \frac{E_e + E'_{\nu}}{2m_p} \tan(\theta_e/2).
\]

Here, \( P'_e \) and \( P'_\mu \) are the transferred polarizations, transverse and longitudinal to the proton momentum (see \(^{[10]}\)). The beam energy is \( E_e \), the energy (angle) of the scattered electron is \( E'_{\nu} \) (\( \theta_e \)), and \( m_p \) is the proton mass. This relation was used to extract \( G_E/G_M \) for the proton (most recently in \(^{[11,12,13]}\)).

In the following, the results of recent \(^4\text{He}(e, e'p)\) experiments to study the proton knock-out process will be discussed. In these experiments \(^4\text{He} \) was chosen as target because of its high density and relatively simple structure, which allows for RDWIA and microscopic calculations.
The kinematics of these experiments, quasielastic scattering at low missing momentum with symmetry about the three-momentum-transfer direction, minimize conventional many-body effects, as will be demonstrated below.

2 Experiments

The first $^4$He polarization-transfer measurement was performed at the Mainz microtron (MAMI) at a four-momentum squared $Q^2 = 0.4 \, (\text{GeV}/c)^2$ [14]. More recently these measurements were extended to $Q^2 = 0.5, 1.0, 1.6,$ and $2.6 \, (\text{GeV}/c)^2$ in experiment E93-049 at Jefferson Lab Hall A [15, 16]. Since these experiments were designed to detect differences between the in-medium polarizations compared to the free values, both $^4$He and $^1$H targets were employed (due to beam-time constraints, only produced polarization, polarization ratio measured in the identical setting: $^4$He polarization ratio is normalized to the hydrogen polarization ratio). The proton-recoil polarization observables were extracted by means of the focal-plane polarimeter (FPP). The proton-recoil distribution of protons scattered off the graphite analyzer was found to be in excellent agreement with previous data in experiment E93-049 at Jefferson Lab Hall A [16]. Since these experiments were recently performed in experiment E93-049 at Jefferson Lab Hall A [15, 16].

In each experiment, two high-resolution spectrometers were used, one to detect the scattered electron and one to detect the recoiling proton. The latter was equipped with a focal-plane polarimeter (FPP). The proton-recoil-polarization observables were extracted by means of the maximum-likelihood technique, utilizing the azimuthal distribution of protons scattered off the graphite analyzer in the FPP.

The results of the measurements are expressed in terms of the polarization-transfer double ratio, in which the helium polarization ratio is normalized to the hydrogen polarization ratio measured in the identical setting:

$$R = \frac{(P'_{y}/P''_{y})^{4}\text{He}}{(P'_{y}/P''_{y})^{^1}\text{H}}. \quad (2)$$

As a cross-check, the hydrogen results were also used to extract the free-proton form-factor ratio $G_E/G_M$, which was found to be in excellent agreement with previous data [11,12]. Nearly all systematic uncertainties cancel in $R$: the polarization-transfer observables are to first order independent of instrumental asymmetries in the FPP, and their ratio is independent of the electron-beam polarization and carbon analyzing power. Small systematic uncertainties are predominantly due to uncertainties in the spin transport through the proton spectrometer.

3 Results

Figure 1 shows the results for $R$ at $Q^2 = 1.0 \, (\text{GeV}/c)^2$ as a function of missing momentum. The five data points correspond to five bins in the acceptance within the single experimental setting. Negative values of missing momentum correspond to the recoiling nuclei having a momentum component antiparallel to the direction of the three-momentum transfer.

The data are compared with several calculations, which were averaged over the experimental acceptance. In the relativistic calculations by the Madrid group [17], the Coulomb gauge and the current operator cc1 [20] were used. The dotted line is a result of a calculation in plane-wave impulse approximation (RPWIA). This calculation predicts $R \approx 1$ at $p_m = 0$. It overpredicts the data by about 10%, although the missing-mass distribution of the data is reasonably well described. The relativistic distorted-wave impulse approximation (RDWIA) gives a smaller value of $R (\approx 3\%)$ than the RPWIA but still overpredicts the data (solid curve). The calculation uses the MRW optical potential of [21]. The main difference in the results between this full calculation and the RPWIA is due to the enhancement of the negative energy components of the relativistic bound and scattered proton wave functions. This can be demonstrated by projecting the wave functions over positive-energy states (dash-dotted curve) resulting in essentially the same polarization-transfer ratio as given by RPWIA. Also, a Glauber calculation by the Gent group [18,19] (long-dashed line) is unable to account for the data.

The induced polarization $P_y$ in the $(e,e'p)$ reaction is identically zero, in the absence of FSI effects (in the one-photon-exchange approximation). This observable thus constitutes a stringent test of various FSI calculations. Figure 2 shows the results, corrected for (small) false asymmetries, as a function of $Q^2$. One sees that the induced polarizations are small for all measured $Q^2$ values.

The dashed and dot-dashed curves constitute RDWIA calculations by the Madrid group [17] with the MRW [21] and RLF [22] relativistic optical potentials. For the induced-polarization case, the RDWIA curves do not depend on the nucleon form-factor model chosen in the calculations. Figure 2 confirms the expected smallness of the induced polarizations, and seems to indicate a reasonable agreement with the RDWIA calculation.

However, due to the relatively large systematic uncertainties caused by possible false asymmetries in the FPP,
Fig. 2. Measured values of the induced polarizations for the 
$^4\text{He}(e,e'p)^3\text{H}$ reaction [16]. The inner uncertainty is statistical
only, the total uncertainty includes a systematic uncertainty
of $\pm 0.02$, due to the imperfect knowledge of the false asymme-
tries. The hatched areas show the results for different RDWIA
calculations [17] with the MRW [21] and RLF [22] relativistic
optical potentials. All theoretical curves are averaged over the
experimental acceptance. Dotted curves indicate calculat-
ions in which the optical potentials were extrapolated beyond the
region of validity.

the test is not conclusive. A far more detailed study of
the induced polarization can be made with data expected
from JLab experiment E03-104 [23].

4 Discussion

The disagreement between the data and the RDWIA cal-
culations for the polarization double ratio $R$ is puzzling,
since, as mentioned earlier, these relativistic calculations
provide good descriptions of, e.g., the induced polariza-
tions measured at Bates in the $^{12}\text{C}(e,e'p)$ reaction [24]
and of $A_{TL}$ in $^{16}\text{O}(e,e'p)$ as previously measured at JLab
[11]. To find a possible explanation for that disagreement,
4a detailed study of model dependencies was performed.

First, the model input in the calculations of the Madrid
group was studied. Figure 3(a) shows again the $Q^2 = 1.0
(GeV/c)^2$ polarization-transfer double-ratio data. The
hatched area indicates the range of different RDWIA cal-
culations. For these calculations, various bound-state wave
functions, current operators ($cc_1$ and $cc_2$), and optical
potentials were chosen. The optical potentials include the
MRW folding parameters [21] and the RLF folding param-
eters [22]. The latter are valid only up to $T_{lab} \approx 400$ MeV,
and thus are already beyond its regime of validity for
$Q^2$ of 1.0 (GeV/c)$^2$. Different optical potentials were con-
structed for each parameter set based upon the experimental
$^3\text{H}$ density, based upon a simple Woods-Saxon density for
$^3\text{H}$ with the same root-mean-square radius as the exper-
imental one, and, finally, one with an 30% increased
root-mean-square radius, resulting in an unrealistic poten-
tial. Different parametrizations of the free-nucleon form
factors were also used. To a very good approximation, the
ratio $R$ is independent of such variations, if the same
parametrization is used in the $^4\text{He}$ and $^1\text{H}$ calculations.
It is evident from Fig. 3(a) that there is hardly any sen-
sitivity in the polarization-transfer double ratio at $Q^2 = 1.0
(GeV/c)^2$ along with a PWIA and different RDWIA calculations of the Madrid group [17]. (b) Relative difference
between the polarization transfer ratio including channel coupling and without channel coupling. The calculation follows the
approach of [25]. (c) Differences in the polarization double ratios relative to $R_{cc1}$ in the $^4\text{He}(e,e'p)^3\text{H}$ reaction as a function
of missing momentum (perpendicular kinematics). Plotted are results for different de Forest current operators with and with-
out the MEC seagull diagram. The 1-body $cc1$ result serves as
a baseline. Calculation courtesy of Meucci [26].

Next, the effect of channel coupling on $R$ for the
$^4\text{He}(e,e'p)^3\text{H}$ reaction was estimated. Recently Kelly
[25]...
investigated the sensitivity of recoil-polarization observables in $A(e,e'p)B$ reactions to channel coupling in final-state interactions (for $^{12}$C and $^{16}$O). In these studies it was found that polarization-transfer observables for proton knockout with modest missing momentum appear to be quite insensitive to details of the final-state interaction, including channel coupling. Following the approach of Kelly et al., the effect of channel coupling was estimated for the $^2$He$(e,e'p)^3$H reaction by calculating the relative difference between the polarization transfer ratio with and without channel coupling. Couplings between the proton $1s_{1/2}$ and neutron $1s_{1/2}$ states were considered. Figure 3(b) shows the results for a four-momentum transfer of $Q^2 = 1.0$ (GeV/c)$^2$. The effect is minimal, and on average is of the order of 1% – 2%.

Finally, the effects of two-body interactions were considered. Available model calculations indicate that these contributions are smallest in quasielastic, parallel kinematics and at low missing momentum; the kinematics of the experiments discussed here. In a recent work, the Pavia group has studied meson-exchange currents in a relativistic model for electromagnetic one-nucleon emission (for $^{12}$C and $^{16}$O). Meucci has provided us with similar calculations for $^4$He; these results are shown in Fig. 3(c) for $Q^2 = 1.0$ (GeV/c)$^2$ as relative differences with respect to the one-body $cc$ calculation. The horizontally hatched band covers the range of calculations with three different one-body currents ($cc1$, $cc2$, $cc3$). The calculations confirm that, at low missing momentum, ambiguities due to the choice of the 1-body current ($cc1$, $cc2$, $cc3$) are small, of the order of 3%. The inclusion of the two-body current in the form of the seagull diagram with one-pion exchange (diagonally hatched band) has an asymmetric effect on the polarization ratio about $p_m = 0$; the effect of MEC is also small. It reduces the polarization transfer ratio by about 2% on average. In addition, these calculations predict the effect of MEC to decrease with increasing four-momentum transfer (not shown).

Also the results of the microscopic calculations of Laget et al. for $Q^2 = 0.4$ (GeV/c)$^2$ and 0.5 (GeV/c)$^2$ were found to be nearly identical to the RPWIA results (see Fig. 5) indicating that reaction mechanisms like MEC, IC, or charge exchange do not contribute significantly to $R$ in the present kinematics.

Does the present failure of state-of-the-art calculations to describe $R$ indicates a breakdown of standard meson-nucleon calculations? Probably not. It is likely that more complete and more complicated many-body calculations eventually will account for the data. Similarly, the observed cross-section scaling in deuteron photodisintegration at high energies (see e.g. [27]) does not “prove” a breakdown of meson-nucleon calculations, but rather indicates the onset of a regime where quark-gluon-inspired models may give a more effective basis for the interpretation of the data. In the same way, the observed reduction of $R$ in the $^4$He$(e,e'p)^3$H reaction motivates the use of a new approach in the interpretation of the data.

Indeed, a calculation by Lu et al. [28], using a quark-meson-coupling (QMC) model, suggests a measurable deviation from the free-space form-factor ratio over the $Q^2$ range $0.0 < Q^2 < 2.5$ (GeV/c)$^2$. Note that the calculation is consistent with present constraints on possible medium modifications for both the electric form factor (from the Coulomb Sum Rule, with $Q^2 < 0.5$ (GeV/c)$^2$ [29,30,31]), and the magnetic form factor (from a $y$-scaling analysis [32], for $Q^2 > 1$ (GeV/c)$^2$), and limits on the scaling of nucleon magnetic moments in nuclei [33]. Similar measurable effects have been calculated in the light-front-constituent quark model of Frank et al. [34]. Recently, Yaksheev et al. [35] investigated possible modifications to the electromagnetic form factors of the nucleons in the $^4$He nucleus in the framework of a modified Skyrme model, up to $Q^2 = 0.6$ (GeV/c)$^2$. Furthermore, the group of Miller is presently studying medium effects in the framework of a chiral soliton model for the proton [36].

However, the notion of medium modification of single-particle properties like, e.g., the electromagnetic form factors of a nucleon, in a nuclear environment is a purely theoretical concept [37]. Thus, distinguishing possible changes in the spatial structure of nucleons embedded in a nucleus from more conventional many-body effects is only possible within the context of a model; presently the RDWIA calculation of the Madrid group.

The RDWIA results are brought into excellent agreement with the data by replacing the free-nucleon form factor with a density dependent, medium-modified form factor based on the QMC model [28] (solid curve in Fig. 4).

A summary of all available $^4$He$(e,e'p)^3$H data is shown in Fig. 5 along with different acceptance-averaged calculations. The polarization-transfer double ratio is plotted as a function of $Q^2$. In order not to obscure the result by small kinematical differences between the individual $^3$H and $^4$He measurements, data and calculations are shown with $R_{PWIA}$ as a baseline. The Mainz data point at $Q^2 = 0.4$ (GeV/c)$^2$ closely coincides with the more recent results at $Q^2 = 0.5$ (GeV/c)$^2$ of JLab.
Fig. 5. Superratio $R/R_{\text{PWIA}}$ as a function of $Q^2$ (closed circles). The dashed line shows the results of the RDWIA calculation of the Madrid group [17]. The dotted line shows the results of the full nonrelativistic model of the Gent group [18, 19]. The dash-dotted line shows the results of the full calculation, including two-body currents, of Laget [8]. The solid line indicates the full relativistic calculation of the Madrid group [17] including medium modifications as predicted by a quark-meson-coupling model [23]. For $Q^2 > 1.8$ (GeV/c)$^2$, the Udis calculations maintain a constant relativistic optical potential and are indicated as short-dashed lines. The lines connecting the acceptance-averaged theory calculations are to guide the eye only. The open circles indicate the projected data for experiment E03-104 [28].

On average, the RPWIA calculation (baseline) overestimates the data by $\approx 10\%$. The dotted line shows the results of the full nonrelativistic model of the Gent group [18, 19]. The full calculation, including two-body currents, of Laget [8] is only available for the lower two $Q^2$ values (dash-dotted). Both calculations are comparable to the results of RPWIA. The RDWIA calculation (dashed curve) gives a slightly smaller value of $R$ but still overpredicts the data.

The inclusion of medium-modified form factors as predicted by Lu et al. [28] into the RDWIA calculation gives a significantly improved agreement with data, with the exception of the datum at $Q^2 = 1.6$ (GeV/c)$^2$ ($\chi^2$ per degree of freedom of 1.3 for the five data points), in contrast to the use of free form factors ($\chi^2$ per degree of freedom of 2.2). All calculations by the Madrid group [17] use the Coulomb gauge, the $c1$ current operator as defined in [24], and the MRW optical potential of [24]. The $c2$ current operator gives higher values of $R$, worsening agreement with the data. As discussed above, various choices for, spinor distortions, current operators, and relativistic corrections affect the theoretical predictions by $\leq 3\%$, and presently cannot explain the disagreement between the data and the RDWIA calculations.

Also shown in Fig. 5 are the projected data points at $Q^2 = 0.8$ (GeV/c)$^2$ and 1.3 (GeV/c)$^2$ for the newly approved JLab experiment E03-104 [28]. This experiment will reduce the statistical uncertainties in the double polarization ratio at each $Q^2$ by over a factor of two compared to the previous measurements. These two $Q^2$ values were selected since they lie in a region where theoretical calculations are expected to be reliable. This measurement will provide one of the most stringent tests to date of the applicability of conventional meson-nucleon calculations.

Any medium modification of bound-nucleon form factors carries implications for the nuclear EMC effect [30]. For example strong constraints are placed on models of the nuclear EMC effect by model-independent relations derived on the basis of quark-hadron duality, which relate the medium modification of the electromagnetic form factors to the modification of the deep-inelastic structure function of a bound proton [38].

5 Summary

Polarization transfer in the quasielastic $(e, e'p)$ reaction is sensitive to possible medium modifications of the bound-nucleon form factor, while at the same time largely insensitive to other reaction mechanisms. The $^4\text{He}(e, e'p)^3\text{H}$ polarization-transfer double-ratio data are not well described by modern relativistic RDWIA calculations using free nucleons as quasiparticles. The data can be efficiently described if medium-modified nucleons are used in the calculations. However, the evidence from the present data is still limited. New high-precision data expected from JLab Hall A should provide a more stringent test of conventional meson-nucleon calculations.

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