Recommendations of the LHC Dark Matter Working Group: Comparing LHC searches for dark matter mediators in visible and invisible decay channels and calculations of the thermal relic density

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ABSTRACT

Weakly-coupled TeV-scale particles may mediate the interactions between normal matter and dark matter. If so, the LHC would produce dark matter through these mediators, leading to the familiar “mono-X” search signatures, but the mediators would also produce signals without missing momentum via the same vertices involved in their production. This document from the LHC Dark Matter Working Group suggests how to compare searches for these two types of signals in case of vector and axial-vector mediators, based on a workshop that took place on September 19/20, 2016 and subsequent discussions. These suggestions include how to extend the spin-1 mediated simplified models already

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in widespread use to include lepton couplings. This document also provides analytical calculations of the relic density in the simplified models and reports an issue that arose when ATLAS and CMS first began to use preliminary numerical calculations of the dark matter relic density in these models.

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1. Introduction

During the LHC Run-2, ATLAS and CMS searches for dark matter (DM) using missing transverse energy signals have begun to use a common set of simplified models, reviewed by the ATLAS/CMS Dark Matter Forum (DMF), to describe how DM would be produced [1]. The models involve TeV-scale mediating particles that couple to quarks and a Dirac fermion DM candidate. The coupling to DM leads to collision events where a high-energy Standard Model (SM) final state recoils against invisible DM particles. Many types of accompanying SM particles are possible, often arising from initial-state radiation, creating a broad set of possible signals involving missing transverse energy (MET). The coupling to quarks, which permits the LHC to produce the mediating particles, also allows the mediators to decay to jets [2–4] or possible to top-quark pairs [3,5,6]. Such events, which lack substantial MET, could be used to fully or partially reconstruct the mass and other properties of the mediators.

The LHC Dark Matter Working Group (WG), established by ATLAS, CMS, and the LH’Physics Centre at CERN (LPCC) as the successor of the ATLAS/CMS DMF [1], has recommended a set of standardized plots for comparing DM searches that differ in the accompanying SM recoil [7]. The recommendations include depicting the results of these searches in slices of DM mass versus mediator mass for fixed values of the mediator couplings to DM and SM particles. The LHC did not address how these comparisons could incorporate searches for fully-visible decays of the mediators.

As ATLAS and CMS adopted the recommendations for their Run-2 results, both produced preliminary comparisons between visible-decay and invisible-decay searches, starting with an ATLAS comparison of mono-jet, mono-photon, and di-jet searches in the DM-mediator mass plane for a single choice of couplings [8], followed by a comparison of CMS results [9] that were also extrapolated to the DM-nucleon cross section for direct-detection DM searches (see also [10] for updated results on di-jet resonances). Both ATLAS and CMS results also depict values of the mass parameters where the simplified model reproduces the observed DM density in the standard thermal relic scenario.

The present document discusses some of what has been learned while preparing the above results and includes additional recommendations, stemming from the discussion at the public meeting of the WG in September 2016. Section 2 adds couplings to leptons for the s-channel vector and axial-vector simplified models and provides additional benchmark coupling scenarios that illustrate the relationships amongst the various visible and invisible mediator searches. Section 3 discusses a deficiency in the relic density calculations commonly used for the first Run-2 results [7–9] and compares a new computation with version 2.0.6 of MadDM with the results of an analytic calculation.

2. Lepton couplings for simplified DM models

The simplified models recommended by the ATLAS/CMS DMF [1] assume that DM is a Dirac fermion \( \chi \) and there is an additional heavy particle mediating the SM-DM interaction (the “mediator”). In the most basic set of these models, the mediator is a vector, an axial-vector, a scalar or a pseudo-scalar boson. So far, ATLAS and CMS have focused on the subset of the models where the mediator is exchanged in the s-channel. These models contain four free parameters. In the vector and axial-vector models, the parameters are the DM mass \( m_{\text{DM}} \), the mediator mass \( M_{\text{med}} \), the coupling \( g_{\text{DM}} \) of a mediator-DM-DM vertex, and the coupling \( g_\chi \) of the mediator-quark–quark vertices. In the scalar and pseudo-scalar models, a quark-mass-dependent Yukawa factor scales the coupling of the mediator-quark–quark vertices to avoid violating flavour constraints. These four quantities parameterize the production rate of the mediator in proton–proton collisions, its quark and DM decay rates, and the kinematic distributions of signal events.

Complete models of DM can contain mediators that may have (or require for consistency) couplings to other SM particles that are not found in the simplified models above. Such couplings would introduce additional decay modes of the mediator at the LHC as well as further DM annihilation channels in the relic density calculation. In this section, we discuss why and how to add lepton couplings to the vector and axial-vector simplified models, provide formulae for the total decay width of the mediators, and discuss the implementation of these models that are currently available. We then propose four benchmark scenarios for comparing di-jet, di-lepton, and mono-X searches, based on rough estimates of the sensitivity of these searches with 30 fb\(^{-1}\) of LHC data. We also comment on the interference between the mediator di-lepton process and the Drell–Yan backgrounds to di-lepton searches. We postpone the discussion of scalar and pseudo-scalar models to a future document.

2.1. Charged lepton couplings in vector and axial-vector simplified models

Simplified models are designed to capture the coarse details of collider phenomenology found in complete, rigorously-derived theories of new physics, without the attendant complexity of the full theory, particularly at energies scales that cannot be accessed at the collider. The ATLAS/CMS DMF focused on the phenomenology of MET signatures at the LHC. In the simplified DMF models involving spin-1 mediators, \( \ell \) quark couplings provide \( pp \) collider production, and DM couplings provide the decays to DM. These two couplings set a “minimal width” for the spin-1 resonance.

When adapting the simplified DMF models to the phenomenology of fully-visible signatures, one should more closely consider the effects of the additional couplings. Among these, couplings to charged leptons are often found or even required in complete theories. They are sometimes necessary in order to construct a consistent theory, for example in minimal completions of the axial-vector model [11,12] or in models with extended Higgs sectors [13,14]. They often appear in anomaly-free spin-1 mediator models [15], see also Section 3.3.2 of [7]. They may also be induced through radiative corrections (e.g. through quark loops that lead to \( Z^\prime–Z \) mixing). The near-ubiquity of lepton couplings in full theories motivates including them when searching for visibly-decaying spin-1 mediators.

The DMF spin-1 simplified models can be easily extended with couplings to charged leptons \( g_\ell \), equal for all lepton flavours.

\(^1\) In this document, we will focus on the case of spin-1 mediators, and postpone the discussion of scalar and pseudo-scalar mediators to future work.
Assuming that the new interactions conserve parity, mediator vertices with leptons will have the same Lorentz structure as the vertices with quarks. We then obtain the following interaction Lagrangians for the vector and axial-vector $Z'$ mediator models:

$$\mathcal{L}_{\text{vector}} = -g_{\text{DM}} Z'_\mu \tilde{\chi} \chi^\mu - g_q \sum_{q=u,d,s,c,b,t} Z'_\mu \tilde{q} q^\mu,$$

$$\mathcal{L}_{\text{axial-vector}} = -g_{\text{DM}} Z'_\mu \tilde{\chi} \gamma_5 \chi - g_q \sum_{q=u,d,s,c,b,t} Z'_\mu \tilde{q} q^\mu \gamma_5,$$  \hspace{1cm} (1)

Notice that the generation-universality of the couplings $g_q$ and $g_{\text{DM}}$ guarantees that these spin-1 models are consistent with --- but more restrictive than --- the minimal flavour violation (MFV) assumption [16], imposed to evade constraints from flavour physics.

Adding lepton couplings allows the mediator to decay to charged lepton pairs at tree level. For many values of $g_q$, this will lead to stringent bounds from searches for di-lepton resonances.

### 2.2. Neutrino couplings in vector and axial-vector simplified models

Following the reductionist philosophy of simplified models, the DMF did not build strict theoretical self-consistency into its models. For example, the simplified models do not specify how the $Z'$ boson acquires a mass nor does the formulation of the models explicitly require gauge invariance. When adjusting the focus of the simplified models beyond mono-jet like searches to also include direct searches for the mediators, neglecting these aspects becomes less justified. While a discussion of mass generation in spin-1 simplified models is beyond the scope of this document, we will in the following explain how gauge invariance restricts the lepton couplings of the spin-1 models.

In the case at hand, gauge invariance requires a relation of the couplings of the spin-1 mediator to charged leptons and the left-handed neutrinos. For both the vector and the axial-vector model, the Lagrangian that describes relevant neutrino interactions for each neutrino flavour takes the form:

$$\mathcal{L}_\nu = -g_\nu \sum_{i=e,\mu,\tau} Z_i^\nu \tilde{\nu}_i \frac{1}{2} (1 - \gamma_5) \nu_i.$$  \hspace{1cm} (3)

The relation required between $g_\nu$ and $g_i$ differs in the two models. For the vector model, $g_\nu = g_\nu$, whereas for the axial-vector model, $g_\nu = -g_i$. Because right-handed neutrinos are absent in the SM, the mediator to neutrinos necessarily breaks parity and therefore has a different Lorentz structure from the coupling to charged leptons.

The new coupling $g_\nu$, implied by gauge invariance, has an important consequence for the phenomenology of MET searches: it supplies an additional invisible decay channel, which may enhance certain mono-X signals.

### 2.3. Width formulae and model implementation

Including leptonic couplings the partial decay widths of the vector mediator are given by

$$\Gamma_{\text{vector}}^{\nu\bar{\nu}} = \frac{g_{\text{DM}}^2 M_{\text{med}}}{12\pi} (1 - 4z_{\text{DM}})^{1/2} (1 + 2z_{\text{DM}}),$$

$$\Gamma_{\text{vector}}^{\ell\bar{\ell}} = \frac{g_{\text{DM}}^2 M_{\text{med}}}{12\pi} (1 - 4z_{\text{DM}})^{1/2} (1 + 2z_{\text{DM}}),$$

$$\Gamma_{\text{vector}}^{\nu\bar{\nu}} = \frac{g_i^2 M_{\text{med}}}{24\pi} z_i,$$  \hspace{1cm} (4)

$$\Gamma_{\text{vector}}^{\ell\bar{\ell}} = \frac{g_i^2 M_{\text{med}}}{12\pi} (1 - 4z_i)^{1/2} (1 + 2z_i),$$

$$\Gamma_{\text{vector}}^{\nu\bar{\nu}} = \frac{g_i^2 M_{\text{med}}}{24\pi} z_i,$$  \hspace{1cm} (5)

where $z_i = m_i^2 / M_{\text{med}}^2$ with $i = \text{DM}, q, \ell$, and the three different types of contributions to the decay width vanish for $M_{\text{med}} < 2m_i$. The corresponding expressions for the axial-vector mediator are

$$\Gamma_{\text{axial-vector}}^{\nu\bar{\nu}} = \frac{g_{\text{DM}}^2 M_{\text{med}}}{12\pi} (1 - 4z_{\text{DM}})^{3/2},$$

$$\Gamma_{\text{axial-vector}}^{\ell\bar{\ell}} = \frac{g_i^2 M_{\text{med}}}{4\pi} (1 - 4z_i)^{3/2},$$

$$\Gamma_{\text{axial-vector}}^{\nu\bar{\nu}} = \frac{g_i^2 M_{\text{med}}}{12\pi} (1 - 4z_i)^{3/2},$$

$$\Gamma_{\text{axial-vector}}^{\ell\bar{\ell}} = \frac{g_i^2 M_{\text{med}}}{24\pi} z_i.$$  \hspace{1cm} (6)

Chapter 4 of the ATLAS/CMS DMF report [1] provides guidelines for simulating the models it discusses, along with a reference implementation [17]. Another more recent implementation of the spin-1 DMF models that provides next-to-leading order plus parton shower accuracy in the MadGraph5_aMCNLO framework [18] has been presented in [19]. The corresponding UFO file [20] has been obtained with FeynRules 2 [21] and can be found at [22]. The original implementation has been modified to include the lepton couplings discussed above.

#### 2.3.1. Benchmark scenarios for simplified models with lepton couplings

In an earlier document [7], this WG recommended a set of standardised plots for comparing results from different MET search channels in these models, including depicting the search results in slices of DM mass versus mediator mass for fixed values of the mediator couplings to DM and SM particles. Because in the spin-1 case the differences in the various signals arise from initial state radiation, their rates relative to one another are fixed by SM couplings, not the new couplings entering the simplified model. When using the same plots for subsequent comparisons with searches for fully-visible signatures, whose signal rates relative to the invisible channels do depend on the couplings in the simplified model, albeit in straightforward ways, it becomes crucial to convey how the relative strength of each search varies with the choice of couplings.

To solve this problem, the strategy employed by ATLAS and CMS has been to show slices of DM mass versus mediator mass for one or more sets of “benchmark” coupling values that illustrate the complementary strengths of the different searches, as in [7–9]. When introducing lepton couplings, we recommend the following four scenarios with different relative sizes of quark and lepton couplings:

- **V1**: Vector model with couplings only to quarks: $g_{\text{DM}} = 1.0$, $g_q = 0.25$, $g_i = 0$.
- **V2**: Vector model with a small couplings to leptons: $g_{\text{DM}} = 1.0$, $g_q = 0.1$, $g_i = 0.01$.
- **A1**: Axial-vector model with couplings only to quarks: $g_{\text{DM}} = 1.0$, $g_q = 0.25$, $g_i = 0$.
- **A2**: Axial-vector model with equal couplings to quark and leptons: $g_{\text{DM}} = 1.0$, $g_q = g_i = 0.1$.

Scenarios V1 and A1 are the simplified models already in use. Scenario A2 represents a representative case found in the simplest complete models with axial-vector $Z'$ bosons [11], and
illustrates the typical impact of searches for di-lepton resonances in these models. When the mediator is a pure vector, however, one can find \( g_\ell < g_1 \). This is for example the case if the mediator couples only to quarks (and DM) at tree-level and obtains couplings to leptons only from mixing with the neutral SM gauge bosons at loop-level. In such a scenario one naturally expects \( g_\ell / g_1 = O(0.1) \) [23] with the precise value of the ratio depending on the exact model realization. Scenario V2 provides a benchmark for this plausible but more pessimistic (from the di-lepton point of view) possibility. The specific value, \( g_\ell = 0.1g_1 \), is chosen so that searches for di-jet and di-lepton resonances will have comparable sensitivity. The contribution to the signal width from neutrino couplings is negligible in both scenarios A2 and V2, and it can be ignored.

Because LHC searches become sensitive to smaller production cross sections as data are collected, it is also meaningful to consider smaller values of \( g_\ell \) (and hence \( g_1 \)) with respect to the initial Run-2 benchmarks. For 30 fb\(^{-1}\) of data, we recommend \( g_\ell = 0.1 \) (and \( g_{DM} = 1 \)). For this smaller quark coupling, with \( g_\ell = 0.1 \) for Scenario A2 and \( g_\ell = 0.01 \) for V2, the total decay width of the mediator is up to 3.2\%.

To consider broader mediator widths while at the same time further suppressing constraints from searches for resonant two-body decays, it may also be interesting to consider larger values of \( g_{DM} \). For example, the spin-1 models are still well within the perturbative regime for \( g_{DM} = 2 \), predicting a mediator width of only 6\% (for \( g_\ell = g_1 = 0.1 \)).

2.4. Interference effects in di-lepton searches

Both the ATLAS and the CMS collaboration have already conducted detailed searches with Run-1 and Run-2 data for massive di-lepton resonances, using assorted spin-1 models [24–28]. These searches have concentrated on narrow resonant signals in the di-lepton invariant mass spectrum \( \sigma / dM_{\ell\ell} \), where one can ignore interference effects between the signal and the SM Drell–Yan background. Such interference effects cannot be neglected in these searches if they significantly modify the size of the signal or distort its shape.

To assess the size of interference effects for the four benchmark scenarios introduced in the previous section, we have re-calculated \( \sigma / dM_{\ell\ell} \) before and after taking the interference into account. The benchmark model with the largest relative width \( \Gamma_{med}/M_{med} \) is scenario A2 with \( g_\ell = g_\ell = 0.1 \). Setting \( g_{DM} = 2 \) to exacerbate the effects of width in this scenario, we still find that the interference effects never exceed 5\% when \( \sigma / dM_{\ell\ell} \) is integrated between \( m_{\ell\ell} \in [M_{med} - 5\Gamma_{med}, M_{med} + 5\Gamma_{med}] \).

The same conclusion holds when the di-lepton pairs are required to pass the selections imposed in the ATLAS and CMS dilepton searches [26,27]. Therefore we suggest such effects can be neglected when setting limits on the parameter space of spin-1 s-channel simplified models.\(^3\) We find worth mentioning, however, that for simplified models spin-0 s-channel mediators, interference effects are instead relevant in \( t\bar{t} \) searches [5,6,29–36].

3. Relic density

In the standard thermal relic “freeze-out” picture of the early Universe, the annihilation rate of DM particles into normal matter determines the temperature at which DM decouples from thermal equilibrium and sets the DM density observed today. One can use the simplified models discussed in Section 2 to predict the relic density and compare with measurements such as the most recent results by the Planck collaboration [37] to gain insight on interesting regions of the model parameter space. In order to do so, one has to make the following assumptions:

- The DM annihilation cross section receives only contributions from the interactions of the simplified model, while possible additional degrees of freedom and couplings not included in the model are irrelevant.
- The DM number density in the Universe today is entirely determined by the DM annihilation cross section predicted by the simplified model. In particular, no additional mechanisms exist that enhance or deplete the relic density.

It is important to realize that if one or both of these assumptions are violated there is no strict correlation between the relic density and the strength of mono-X signals. For instance, if DM is overproduced, the relic density can be reduced if the DM has large annihilation cross sections to new hidden sector states. These states might however not be directly accessible at LHC energies. Conversely, the correct DM relic density can still be obtained if the DM is underproduced. For instance, if the hidden sector carries an antiparticle–particle asymmetry (similar to the baryon asymmetry) then this necessarily leads to a larger relic density compared to the conventional freeze-out picture.

In this section, we assume that the two aforementioned assumptions are satisfied, and present an analytic calculation of the relic density for the dominant annihilation processes that involve spin-0 and spin-1 mediators. We then provide numerical computations of the relic density for the scalar, pseudo-scalar, vector, and axial-vector simplified model scenarios using version 2.0 of the DMSimpL model implementation [22] and version 2.0.6 of MadDM [38,39]. The Lagrangians for these models can be found in [7] and references therein.

For concreteness the coupling values recommended for the first Run-2 results by the ATLAS/CMS DMF are used in this section. The couplings of the spin-1 mediator (vector or axial-vector) to SM quarks is chosen to be \( g_\ell = 0.25 \) and the lepton coupling value is set to zero, corresponding to scenarios V1 and A1 of Section 2.1. The coupling value of the spin-0 mediator (scalar or pseudo-scalar) to quarks is chosen to be \( g_\ell = 1.0 \) with an implicit Yukawa scaling for all SM quarks. For both models, the coupling value of the mediator to DM particles is fixed to be \( g_{DM} = 1 \). A complete set of relic density curves can be found in the LHC DM WG repository [40].

3.1. Analytic expressions for the DM relic density

Fig. 1 shows the two types of Feynman diagrams that are most important in the calculation of the relic density in the simplified models. The graph on the left-hand side illustrates DM annihilation through a single mediator in the s-channel, while the diagram on the right corresponds to DM annihilation to pairs of mediators via the t-channel. For \( M_{med}/2 > m_{DM} \), the s-channel process dominates, while the t-channel process gives the main contribution when the mediators can go on-shell, that is for \( M_{med} < m_{DM} \). For some choices of mediator, e.g. the pseudo-scalar simplified model, higher order processes such as annihilation into three or more mediators are also important if they are kinematically accessible [41].

Analytic expressions for the annihilation cross sections can be derived separately for both Feynman diagrams in Fig. 1. In the case of the s-channel graphs we obtain

\[
\sigma_{ann,s} \propto v = \sum_q N_q^2 \delta_{qDM} \frac{g_\ell^2 g_{DM}^2 M_{DM}^2 - m_q^2}{16\pi (M_{med}^2 - 4m_{DM}^2)\left(M_{med}^2 - m_q^2\right)^2 + M_{med}^2 r_{med}^2} \leq v^2.
\]
\[ \sigma_{\text{ann},s}^p \cdot v = \sum_q \frac{N_q^2 g_{\text{DM}}^2 q^2}{4\pi} \frac{m_{\text{DM}}^2}{(m_{\text{med}}^2 - 4m_{\text{DM}}^2)^2 + M_{\text{med}}^2 r_{\text{med}}^2}, \]

\[ \sigma_{\text{ann},s}^v \cdot v = \sum_q \frac{N_q^2 g_{\text{DM}}^2 q^2}{2\pi} \frac{2m_{\text{DM}}^2 + m_q^2}{(M_{\text{med}}^2 - 4m_{\text{DM}}^2)^2 + M_{\text{med}}^2 r_{\text{med}}^2}, \]

\[ \sigma_{\text{ann},s}^A \cdot v = \sum_q \frac{N_q^2 g_{\text{DM}}^2 q^2}{2\pi} \frac{m_q^2 (4m_{\text{DM}}^2 - M_{\text{med}}^2)^2}{M_{\text{med}}^4 (M_{\text{med}}^2 - 4m_{\text{DM}}^2)^2 + M_{\text{med}}^2 r_{\text{med}}^2}, \]

where the sum includes all quarks with \( m_q \leq m_{\text{DM}} \), \( N_q^2 = 3 \), \( \beta_q = \sqrt{1 - m_q^2/m_{\text{DM}}^2} \) and \( v \) is the relative velocity of the DM pair. Notice that in the pseudo-scalar, vector, and axial-vector case the s-channel annihilation cross section proceeds via s-wave, i.e. it is of \( O(v^0) \), while in the case of scalar exchanges DM annihilation is p-wave suppressed, i.e. it is of \( O(v^2) \). The corresponding annihilation cross sections into charged leptons can be obtained from the above expressions by a suitable replacement of colour factors and SM fermion masses.

In the case of the t-channel diagrams we instead find the following annihilation cross sections

\[ \sigma_{\text{ann},t}^\phi \cdot v = \frac{\sigma_{\text{ann}}^\phi}{24\pi} \frac{m_{\text{DM}}^2 (9m_{\text{DM}}^4 - 8m_{\text{DM}}^2 M_{\text{med}}^2 + 2M_{\text{med}}^4)}{M_{\text{med}}^2 - 2m_{\text{DM}}^2} v^2, \]

\[ \sigma_{\text{ann},t}^\rho \cdot v = \frac{\sigma_{\text{ann}}^\rho}{24\pi} \frac{m_{\text{DM}}^2 (m_{\text{med}}^2 - M_{\text{med}}^2)^2}{M_{\text{med}}^2 - 2m_{\text{DM}}^2} v^2, \]

\[ \sigma_{\text{ann},t}^V \cdot v = \frac{\sigma_{\text{ann}}^V}{4\pi} \frac{m_{\text{DM}}^2 (m_{\text{med}}^2 - M_{\text{med}}^2)^2}{M_{\text{med}}^2 - 2m_{\text{DM}}^2} v^2, \]

\[ \sigma_{\text{ann},t}^A \cdot v = \frac{\sigma_{\text{ann}}^A}{4\pi} \frac{m_{\text{DM}}^2 (m_{\text{med}}^2 - M_{\text{med}}^2)^2}{M_{\text{med}}^2 - 2m_{\text{DM}}^2} v^2, \]

for \( M_{\text{med}} \leq m_{\text{DM}} \). Here \( \sigma_{\text{ann}}^\phi = \frac{\sigma_{\text{ann}}^\rho}{24\pi} \frac{m_{\text{DM}}^2 (9m_{\text{DM}}^4 - 8m_{\text{DM}}^2 M_{\text{med}}^2 + 2M_{\text{med}}^4)}{M_{\text{med}}^2 - 2m_{\text{DM}}^2} v^2, \)

\[ \frac{\sigma_{\text{ann}}^\rho}{24\pi} \frac{m_{\text{DM}}^2 (m_{\text{med}}^2 - M_{\text{med}}^2)^2}{M_{\text{med}}^2 - 2m_{\text{DM}}^2} v^2, \]

\[ \frac{\sigma_{\text{ann}}^V}{4\pi} \frac{m_{\text{DM}}^2 (m_{\text{med}}^2 - M_{\text{med}}^2)^2}{M_{\text{med}}^2 - 2m_{\text{DM}}^2} v^2, \]

\[ \frac{\sigma_{\text{ann}}^A}{4\pi} \frac{m_{\text{DM}}^2 (m_{\text{med}}^2 - M_{\text{med}}^2)^2}{M_{\text{med}}^2 - 2m_{\text{DM}}^2} v^2. \]

Using the velocity expansion\(^4\) \( \sigma_{\text{ann}} \cdot v = a + bv^2 + O(v^4) \) the DM relic density after freeze-out is approximately given by

\[ \Omega h^2 \simeq 0.12 \frac{1.6 \times 10^{-10} \times f_c \text{ GeV}^2}{a + \frac{b}{3} f_c}, \]

where \( f_c = m_{\text{DM}}/T_f \) with \( T_f \) the freeze-out temperature. In our comparison between analytic and numerical results we will employ \( f_c = 28 \). For this value of \( f_c \) the correct relic abundance thus occurs in the ballpark of

\[ 2.2 \cdot 10^{-26} \text{ cm}^3/\text{s} \simeq 4.5 \cdot 10^{-9} \text{ GeV}^{-2} \simeq a + 0.1b. \]

3.2. Numerical results

One can improve upon the analytic calculation described above by performing a numerical calculation that also takes into account the thermal evolution of the Universe. The results presented in this subsection rely on MadDM version 2.0.6. The MadDM package considers all tree-level 2 \( \rightarrow \) 2 interactions between DM and SM particles. The processes are thermally averaged and the resulting relic density is computed. Since MadDM does not yet automatically calculate the mediator width from the model parameters, the DMsmar model was modified to use the mediator width formulae presented for instance in [1,7]. The DM density calculations provided in the previous LHC DM WG recommendations [7] used an earlier version of MadDM which did not include t-channel annihilation to pairs of mediators. Below we will comment on the effects that this omission has.

The panels in Figs. 2 and 3 show the predictions for the relic density \( \Omega h^2 \) in the \( M_{\text{med}} - m_{\text{DM}} \) plane for spin-1 and spin-0 mediators, respectively. In the spin-1 case the coupling scenarios described in Section 2.1 are employed, while for the spin-0 models the standard coupling values \( g_{\text{DM}} = g = 1 \) and \( g_r = 0 \) have been used. The solid contours in all panels indicate the combination of masses for which the correct DM abundance \( \Omega h^2 = 0.118 \) [37] is obtained. The parts in the \( M_{\text{med}} - m_{\text{DM}} \) plane where the relic density is either higher or lower than the observed value are referred to as overabundant and underabundant regions, respectively.

One observes that all models predict an overabundance of DM for \( M_{\text{med}} \gg m_{\text{DM}} \). While the shape and exact size of this region depend on the specific model realization, larger quark couplings \( g_r \) in general allow DM to annihilate into SM particles more efficiently, which reduces the parameter space over which overabundance can occur.

For the vector scenario V1 (top left panel in Fig. 2) only a single overabundant region with \( M_{\text{med}} \gg m_{\text{DM}} \) is present. For the shown part of the \( M_{\text{med}} - m_{\text{DM}} \) plane this case is fully consistent with previous results (see e.g. [7,42,43]). In the axial-vector scenario A1 (top right panel in Fig. 2) the overabundance region extends to higher \( m_{\text{DM}} \) values than in scenario V1. Additionally, there is an overabundance region above the diagonal \( m_{\text{DM}} =\)

\(^4\) This expansion breaks down close to an s-channel resonance, making a numerical solution indispensable.
Fig. 2. The relic density $\Omega h^2$ in the $M_{\text{med}}$–$m_{\text{DM}}$ plane predicted by the four spin-1 scenarios described in Section 2.1. All couplings to DM are set to unity ($g_{\text{DM}} = 1.0$). Top left: scenario V1, vector mediator with couplings only to quarks ($g_q = 0.25$). Top right: scenario A1, axial-vector mediator with couplings only to quarks ($g_q = 0.25$). Bottom left: scenario V2, vector mediator with couplings to quarks and small couplings to leptons ($g_q = 0.1$, $g_\ell = 0.01$). Bottom right: scenario A2, axial-vector mediator with equal couplings to quarks and leptons ($g_q = 0.1$, $g_\ell = 0.1$). The contour lines correspond to the region of parameters space where the relic density is consistent with the value $\Omega h^2 = 0.118$.

$M_{\text{med}}/2$. While this region is also present in the corresponding figures of [43] its width in mediator mass is significantly narrower. The observed difference is due to $t$-channel annihilation diagrams that pair up mediators that have not been included in the latter work but are relevant if $M_{\text{med}} < m_{\text{DM}}$.

In both the vector scenario V2 and axial-vector scenario A2 (lower left and right plot in Fig. 2) the relic density is enhanced with respect to the corresponding scenarios V1 and A1. This is a result of the quark couplings being smaller in V2 and A2 than in V1 and A1. Decreasing the quark couplings however reduces the annihilation cross section, which in turn leads to an overabundance of DM for larger parts of the $M_{\text{med}}$–$m_{\text{DM}}$ plane. We add that for scenario V2 with $g_q = 0.01$, DM annihilation into leptons has essentially no effect on $\Omega h^2$. In scenario A2 with $g_\ell = 0.1$ the relic density is instead slightly suppressed in the whole $M_{\text{med}}$–$m_{\text{DM}}$ plane compared to a model with quark couplings only.

Notice finally that in the case of axial-vector mediation, $s$-channel annihilation proceeds via $s$-wave but is helicity suppressed, while for vector mediators no such suppression occurs (cf. (14) and (15)). This feature qualitatively explains why the regions with DM overabundance are typically larger for axial-vector scenarios than for vector models.

For the scalar simplified model (left panel in Fig. 3), the overabundance region for small $m_{\text{DM}}$ is fades out for $m_{\text{DM}}$ values above the top threshold $m_t$, above which annihilation of DM pairs into top-quark pairs is allowed. Additional overabundance regions occur for $M_{\text{med}} > m_{\text{DM}} > M_{\text{med}}/2$, where the upper bound is due to the onset of mediator pair production and the lower bound reflects the resonant enhancement of DM annihilation to SM particle pairs. A region of overabundance at $M_{\text{med}} > m_{\text{DM}}$ in the predictions shown in [43] is now underabundant after including the $t$-channel annihilation contributions.

The pseudo-scalar simplified model (right panel in Fig. 3) is similar to the scalar scenario, with less pronounced regions of overabundance due to the increased annihilation cross section from $s$-channel $s$-wave contributions. Consequently, no regions of overabundance are observed above the top threshold and the triangular region present for the scalar model at $M_{\text{med}}/2 < m_{\text{DM}}$ is reduced in size compared to [43].

3.3. Comparison of analytic results to full numerical calculations

In Fig. 4 we compare the results of the analytic calculations described in Section 3.1 with full numerical results obtained with the packages MadDM and MicrOMEGAs [44]. The left (right) panel shows the contours in the $M_{\text{med}}$–$m_{\text{DM}}$ plane for which $\Omega h^2 = 0.118$ in the case of scalar (axial-vector) interactions for the coupling choices $g_{\text{DM}} = 1$ and $g_q = 1$ ($g_{\text{DM}} = 0.25$). The analytic results are obtained by employing (12) and (16) in the case of the scalar mediator, while (15) and (19) are used for the axial-vector simplified model. In both cases the ratio of the DM mass to freeze-out temperature is fixed to $x_f = 28$ and also the effective number of relativistic degrees of freedom is kept constant across the $M_{\text{med}}$–$m_{\text{DM}}$ plane.
Fig. 3. The relic density $\Omega h^2$ in the $M_{\text{med}} - m_{\text{DM}}$ plane predicted by the scalar (left panel) and pseudo-scalar (right panel) mediator models with couplings $g_{\text{DM}} = g_0 = 1.0$. The contour lines indicate the observed value of the DM relic density $\Omega h^2 = 0.118$.

Fig. 4. Comparison of the analytic calculations described in Section 3.1 with numerical results obtained with MadDM and MicrOMEGAs. In the scalar case (left panel) the exact numerical results have been obtained with version 2.0.6 of MadDM, while for the axial-vector mediator model (right panel) version 4.1.8 of MicrOMEGAs has been used to calculate the relic density. See main text for further details.

From both panels it is evident that in the limiting cases where one of the channels dominates the annihilation cross sections, the analytic calculations are in good agreement with the numerical results obtained either by version 2.0.6 of MadDM (scalar case) or version 4.1.8 of MicrOMEGAs (axial-vector case). We emphasize that an improved agreement between analytic and numerical calculations can be obtained when using thermally-averaged cross sections and a numerically determined freeze-out temperature [45]. In the case of the axial-vector model, we also display the contour line with $\Omega h^2 = 0.118$ using version 2.0.5 of MadDM. This prediction is used as representative of the results of [43] that did not incorporate $t$-channel annihilation contributions. One observes that not taking into account the annihilation contribution (19) leads to an erroneous prediction of overabundance for $M_{\text{med}} < m_{\text{DM}}$. We have also verified that version 2.0.6 of MadDM and version 4.1.8 of MicrOMEGAs lead to compatible result for axial-vector simplified models.

4. Conclusions

Simplified DM models in which the interactions between the visible and the invisible sector are mediated by the exchange of TeV-scale particles represent an interesting class of all possible realizations of physics beyond the SM with a viable DM candidate. In such scenarios the decays of the mediators can lead to final states where DM is accompanied by SM radiation (so-called mono-X events) but also to signatures that feature only SM particles (such as for instance di-jet or di-lepton events). To map out the DM parameter space in a given simplified model comparing and combining the different LHC search strategies is an important task.

This document describes simplified spin-1 models where a $s$-channel mediator couple to DM, quarks, and leptons. Four benchmark scenarios with different relative sizes of quark and lepton couplings are recommended that exemplify the rich phenomenology of the simplified DM model in the mono-jet, di-jet, and di-lepton channels. In this document, benchmark points for the vector and axial-vector mediator models where the mediator width is large have not been considered. Even though these may evade the constraints provided by di-jet and di-lepton resonance searches, LHC searches for non-resonant phenomena in the same final states, such as the ones in [46–49], are sensitive to wide mediators and can be subject of dedicated future studies.

This document also presents improved numerical calculations for the relic density for the dominant annihilation processes that involve spin-0 and spin-1 mediators. The full numerical results are compared to analytical calculations and found to be in good agreement in all cases where the annihilation cross section is dominated by a single channel. It is furthermore shown that the omission of $t$-channel annihilation contributions can lead to parameter regions which feature an erroneous relic overabundance or underabundance.
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