THE FIRST SURVEY OF X-RAY FLARES FROM GAMMA-RAY BURSTS OBSERVED BY SWIFT: SPECTRAL PROPERTIES AND ENERGETICS

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ABSTRACT

GRB observations with Swift produced the initially surprising result that many bursts have large, late-time X-ray flares. The flares were sometimes intense, had rapid rise and decay phases, and occurred late relative to the prompt phase. Many GRBs have had several flares, which were sometimes overlapping. The origin of the flares can be investigated by comparing the spectra during the flares to those of the afterglow and the initial prompt emission. In this work we have analyzed all significant X-ray flares from the first 110 GRBs observed by Swift. Significant X-ray flares (>3σ) were found in 33 of these GRBs, with 77 flares detected. A variety of spectral models have been fit to each flare. We find that the spectral fits sometimes favor a Band function model, which is more akin to the prompt emission than to that of the afterglow. While some flares are approximately as energetic as the prompt GRB emission, we find that the average fluence of the flares is approximately 10 times below the average prompt GRB fluence. We also find that the peak energy of the observed flares is typically in the soft X-ray band, as one might expect due to the X-ray selection of the sample. These results, when combined with those presented in the companion paper on temporal properties of flares, support the hypothesis that many X-ray flares are from late-time activity of the internal engine that spawned the initial GRB, not from an afterglow-related effect.

Subject headings: gamma rays: bursts — X-rays: general

1. INTRODUCTION

Since its launch on 2004 November 20, Swift (Gehrels et al. 2004) has provided detailed measurements of numerous gamma-ray bursts (GRBs) and their afterglows with unprecedented reaction times. As of 2006 January 24, 110 bursts were detected by the Burst Alert Telescope (BAT; Barthelmy et al. 2004). Approximately 93% of these were observed by the narrow-field instruments in less than 200 ks, and most of those were detected within 200 s (the typical reaction time was ~100 s, but occasionally BAT detected a burst that was observationally constrained). The narrow-field instruments are the X-Ray Telescope (XRT; Burrows et al. 2005a) and the Ultraviolet-Optical Telescope (UVOT; Roming et al. 2005). By detecting burst afterglows promptly and with high sensitivity, the properties of the early afterglow and extended prompt emission can be studied in detail for the first time. This also facilitates studies of the transition between the prompt emission and the afterglow. The rapid response of the pointed XRT instrument on Swift has led to the discovery that large X-ray flares are common in GRBs and occur at times well after the initial prompt emission. This paper provides the first survey of the spectral features of a large sample of these X-ray flares.

While there are still many unknown factors related to the mechanisms that produce GRB emission, the most commonly accepted model is that of a relativistically expanding fireball with associated internal and external shocks (Mészáros & Rees 1997). In this model, internal shocks produce the prompt GRB emission. Observationally, this emission typically has a timescale of ~20 s for long bursts and ~0.2 s for short bursts (Meegan et al. 1996). The expanding fireball then shocks the ambient material to produce a broadband afterglow that decays quickly (typically as ~t^{−0.4} with α ~ 1.2 for the nominal afterglow phase). When the Doppler boosting angle of this decelerating fireball exceeds the opening angle of the jet into which it is expanding, a steepening of the light curve (jet break) is predicted (Rhoads 1999). For descriptions of the theoretical models of GRB emission and associated observational properties, see Mészáros (2002), Zhang & Mészáros (2004), Piran (2005), Woosley (1993), and van Paradijs et al. (2000). For descriptions of the observational properties of the overall X-ray light curve, see Zhang et al. (2006), Nousek et al. (2006), O’Brien et al. (2006), and Willingale et al. (2007).

Several authors have suggested reasons to expect continued activity from the internal engine of the GRB after the classical prompt emission time frame. Katz (1997) considered a model in which a magnetized disk around a central black hole could lead to continued energy release in the form of internal shocks. The parameters of this energy release would depend on the complex configuration of the magnetic field and the magnetic reconnection dynamics, but time periods as long as days for the delayed emission were predicted. Proga & Zhang (2006) have speculated that energy release can be repeatedly stopped and restarted at late times by magnetic flux accumulation and subsequent release. Perna et al. (2006) have suggested that the flares from both short and long bursts can be explained in the context of the evolution and fragmentation of a viscous accretion disk. For short bursts, in particular, Dai et al. (2006) have suggested that late flares can be explained by magnetic reconnection events driven by the breakout of magnetic fields from the surface of differentially rotating millisecond pulsars, which resulted from a progenitor compact binary star merger. King et al. (2005) have speculated that episodic
accretion processes could explain continued internal engine activity. These authors expect that fragmentation and subsequent accretion during the collapse of a rapidly rotating stellar core could explain observations of extended prompt emission. In general, the dominant model of an expanding fireball with internal/external shocks (Mészáros & Rees 1997) allows for continued prompt emission, provided that the internal engine is capable of continuing the energy injection.

A few observations prior to Swift have included indications of flaring from GRBs after the prompt GRB emission phase. Watson et al. (2003) used XMM-Newton to detect line emission from GRB 030227 nearly 20 hr after the prompt burst. They inferred continued energy injection at this late time and concluded that a nearly simultaneous supernova and GRB event would require sporadic power output with a luminosity in excess of $10^{45}$ erg s$^{-1}$. Piro et al. (2005) used BeppoSAX to observe two GRBs with relatively small X-ray flares. The X-ray flare times for GRB 011121 and GRB 011211 were reported as $t = 240$ and 600 s, respectively. The spectral parameters of these two X-ray flares were consistent with afterglow parameters, and these flares were interpreted as the onset of the afterglow (Piro et al. 2005).

Two other examples of flaring and/or late timescale emission can be found in the XMM-Newton observations (Burrows et al. 2005b) provided the initial report that two bursts detected by Swift showed strong X-ray flares. The first of these, XRF 050406, was an X-ray flash with a short and relatively weak X-ray flare that peaked 213 s after $T_0$ of the prompt GRB emission. Due to the fast rise/decay, the most natural explanation for this flare is continued internal engine activity at late times (i.e., delayed prompt emission). XRF 050406 was analyzed in detail by Romano et al. (2006). Another burst, GRB 050502B, was studied in detail by Falcone et al. (2006), since it was the first dramatic, high-fluence X-ray flare detected. This flare, which peaked

| TABLE 1—Continued |
|---|---|---|---|---|
| GRB | Flare | $t_{\text{start}}$ (s) | $t_{\text{stop}}$ (s) | $t_{\text{peak}}$ (s) | S/N |
| 051117a | 1 | 2 | 4322 | 157 | 117.6 |
| 051227 | 1 | 1 | 2 | 134 | 2794 | 380 | 124.1 |
| 05106 | 1 | 3 | 292 | 1313 | 628 | 70.4 |
| 05106 | 1 | 4 | 574 | 2695 | 926 | 78.6 |
| 05106 | 1 | 5 | 642 | 1820 | 1097 | 71.0 |
| 05106 | 1 | 6 | 1237 | 3119 | 1335 | 95.3 |
| 05106 | 1 | 7 | 659 | 3126 | 1535 | 85.8 |
| 051108 | 1 | 1 | 115 | 152 | 132 | 4.4 |
| 051108 | 1 | 2 | 86 | 245 | 120 | 16.7 |
| 051108 | 1 | 3 | 193 | 429 | 285 | 2.1 |
| 051009 | 1 | 4 | 4305 | 6740 | 4810 | 5.0 |
| 051111a | 1 | 2 | 27 | 196 | 110 | 51.5 |
| 051115 | 1 | 2 | 109 | 203 | 171 | 38.6 |
| 051115 | 1 | 3 | 215 | 433 | 312 | 107.4 |
| 05104 | 1 | 1 | 101 | 155 | 111 | 11.7 |
| 05104 | 1 | 2 | 155 | 210 | 168 | 3.2 |
| 05104 | 1 | 3 | 285 | 382 | 374 | 19.2 |
| 05104 | 1 | 4 | 155 | 211 | 177 | 11.2 |
| 05104 | 1 | 5 | 315 | 483 | 385 | 13.2 |
| 05104 | 1 | 6 | 78 | 230 | 120 | 102.6 |
| 05104 | 1 | 7 | 63 | 342 | 261 | 33.7 |
| 05104 | 1 | 8 | 13406 | 402320 | 55783 | 19.7 |
| 05104 | 1 | 9 | 151 | 195 | 162 | 3.0 |
| 05104 | 1 | 10 | 219 | 324 | 274 | 12.2 |
| 05104 | 1 | 11 | 210 | 280 | 228 | 20.6 |
| 05104 | 1 | 12 | 323 | 611 | 435 | 51.9 |
| 05104 | 1 | 13 | 611 | 795 | 678 | 33.7 |
| 05104 | 1 | 14 | 9654 | 12578 | 10319 | 33.2 |
| 05104 | 1 | 15 | 312 | 457 | 435 | 3.8 |
| 05104 | 1 | 16 | 513 | 879 | 753 | 5.8 |
| 05104 | 1 | 17 | 889 | 1516 | 1116 | 4.3 |
| 05104 | 1 | 18 | 4455 | 5703 | 5367 | 5.8 |
| 05104 | 1 | 19 | 7345 | 27698 | 22669 | 14.2 |
| 05104 | 1 | 20 | 7646 | 13093 | 11613 | 14.0 |
| 05104 | 1 | 21 | 16240 | 27698 | 18873 | 5.1 |
| 05104 | 1 | 22 | 1133 | 1974 | 1350 | 3.0 |
| 05104 | 1 | 23 | 1633 | 2577 | 2138 | 6.1 |
| 05104 | 1 | 24 | 56 | 253 | 174 | 11.5 |
| 05104 | 1 | 25 | 9094 | 36722 | 19733 | 6.2 |
| 05104 | 1 | 26 | 200 | 382 | 234 | 66.6 |
| 05104 | 1 | 27 | 212 | 276 | 240 | 8.4 |
| 05104 | 1 | 28 | 390 | 758 | 433 | 50.9 |
| 05104 | 1 | 29 | 343 | 570 | 463 | 41.6 |
| 05104 | 1 | 30 | 857 | 1141 | 953 | 3.0 |
| 05104 | 1 | 31 | 1149 | 1343 | 1235 | 4.2 |
| 05104 | 1 | 32 | 5085 | 9001 | 6765 | 23.0 |
| 05104 | 1 | 33 | 16153 | 24866 | 17329 | 22.1 |
| 05104 | 1 | 34 | 18383 | 38613 | 24156 | 19.5 |
| 05104 | 1 | 35 | 25618 | 30978 | 29392 | 21.6 |
| 05104 | 1 | 36 | 129 | 306 | 145 | 7.3 |
| 05104 | 1 | 37 | 339 | 944 | 404 | 14.0 |
| 05104 | 1 | 38 | 55 | 170 | 111 | 14.3 |
| 05104 | 1 | 39 | 16755 | 32357 | 18898 | 20.1 |
| 05104 | 1 | 40 | 357 | 435 | 377 | 12.1 |
| 05104 | 1 | 41 | 476 | 560 | 497 | 5.6 |
| 05104 | 1 | 42 | 630 | 1541 | 827 | 39.4 |
| 05104 | 1 | 43 | 115 | 148 | 132 | 9.6 |
| 05104 | 1 | 44 | 132 | 201 | 162 | 7.5 |
| 05104 | 1 | 45 | 330 | 749 | 495 | 7.5 |
| 05104 | 1 | 46 | 374 | 1940 | 483 | 3.1 |
| GRB          | FLARE | $t_{\text{begin}}$ (s) | $t_{\text{end}}$ (s) | ($^{(1)}$)$t_{\text{begin}}$ (s) | ($^{(1)}$)$t_{\text{end}}$ (s) | ($^{(2)}$)$t_{\text{begin}}$ (s) | ($^{(2)}$)$t_{\text{end}}$ (s) | ($^{(3)}$)$t_{\text{begin}}$ (s) | ($^{(3)}$)$t_{\text{end}}$ (s) |
|-------------|-------|------------------------|-----------------------|-----------------------------------|-----------------------------------|-----------------------------------|-----------------------------------|-----------------------------------|-----------------------------------|
| 050219a     | 01    | 118                    | 453                   | 670                               | 29,603                            | ...                                | ...                                | ...                                | ...                                |
| 050406      | 01    | 139                    | 361                   | 1447                              | 919,330                           | ...                                | ...                                | ...                                | ...                                |
| 050421      | 01    | 136                    | 165                   | 167                               | 488                               | ...                                | ...                                | ...                                | ...                                |
| 050502b     | 02    | 410                    | 1045                  | 5384                              | 20,369                            | 161,890                            | 299,820                           | ...                                | ...                                |
| 050607      | 03    | 94                     | 255                   | 92                                | 94                                | 685                                | 20,997                            | ...                                | ...                                |
| 050712      | 02    | 88                     | 299                   | 5157                              | 105,060                           | ...                                | ...                                | ...                                | ...                                |
| 050713a     | 03    | 415                    | 590                   | 5074                              | 63,858                            | ...                                | ...                                | ...                                | ...                                |
| 050714b     | 04    | 788                    | 952                   | 5074                              | 63,858                            | ...                                | ...                                | ...                                | ...                                |
| 050716      | 02    | 155                    | 211                   | 105                               | 155                               | 211                                | 331                               | ...                                | ...                                |
| 050724      | 03    | 78                     | 230                   | 433                               | 27,350                            | ...                                | ...                                | ...                                | ...                                |
| 050726      | 04    | 222                    | 342                   | 433                               | 27,350                            | ...                                | ...                                | ...                                | ...                                |
| 050730      | 05    | 611                    | 795                   | ...                               | ...                               | ...                                | ...                                | ...                                | ...                                |
| 050802      | 06    | 513                    | 879                   | 34,808                            | 778,510                           | ...                                | ...                                | ...                                | ...                                |
| 050803      | 07    | 889                    | 1516                  | 34,808                            | 778,510                           | ...                                | ...                                | ...                                | ...                                |
| 050814      | 08    | 4455                   | 5703                  | 34,808                            | 778,510                           | ...                                | ...                                | ...                                | ...                                |
| 050819      | 09    | 7345                   | 27,698                | 34,808                            | 778,510                           | ...                                | ...                                | ...                                | ...                                |
| 050820a     | 10    | 10,396                 | 13,093                | 34,808                            | 778,510                           | ...                                | ...                                | ...                                | ...                                |
| 050822      | 11    | 17,240                 | 27,698                | 34,808                            | 778,510                           | ...                                | ...                                | ...                                | ...                                |
| 050823      | 12    | 9,654                  | 12,578                | 4366                              | 6863                              | 26,422                             | 99,149                            | ...                                | ...                                |
| 050904      | 13    | 312                    | 457                   | 494                               | 2873                              | ...                                | ...                                | ...                                | ...                                |
| 050908      | 14    | 513                    | 879                   | 34,808                            | 778,510                           | ...                                | ...                                | ...                                | ...                                |
| 050915a     | 15    | 273                    | 391                   | 683                               | 13,093                            | ...                                | ...                                | ...                                | ...                                |
| 051016      | 16    | 9,654                  | 12,578                | 4366                              | 6863                              | 26,422                             | 99,149                            | ...                                | ...                                |
740 s after the prompt GRB emission, released as much energy in the X-ray band as the prompt GRB released in the 15–150 keV band. Following these two GRBs with flares, it became clear that this was a common feature of GRBs, as more and more *Swift* bursts displayed X-ray flares. Although there are a few interesting cases of optical flares and of flares simultaneous with higher energy emission detected by the *Swift* BAT, most of these X-ray flares were generally not accompanied by either optical or 15–150 keV emission at a detectable level. This implied that the peak of the emission was generally in the soft X-ray band.

There have been several papers studying individual GRBs with X-ray flares (Burrows et al. 2005b; Falcone et al. 2006; Romano et al. 2006; Pagani et al. 2006; Cusumano et al. 2007; Zhang et al. 2006; Morris et al. 2007; Goad et al. 2007; Krimm et al. 2007).

While the detailed study of individual flares is important, it is equally important to study the properties of the flares in a more general sense to look for general trends and overall mean properties of the flares. By comparing these overall properties to those of the prompt GRB emission and the afterglow emission, the mechanism of the flare emission may be elucidated. Furthermore, we can see if there are multiple classes of flares or if the flare parameters all fall into one uniform distribution.

In this paper and a companion paper (Chincarini et al. 2007, hereafter Paper I) we present the first temporal and spectral study of a statistical sample of X-ray flares in GRBs. Paper I presents the temporal properties of the sample, and this paper presents the spectral properties of the sample. The sample includes all bursts, up until 2006 January 24, for which *Swift* detected at least one significant X-ray flare.

### Table 2—Continued

| GRB     | Flare | $t_{\text{begin}}$ (s) | $t_{\text{end}}$ (s) | ($\lambda$) | ($\lambda$) | ($\lambda$) | ($\lambda$) | ($\lambda$) |
|---------|-------|------------------------|-----------------------|-------------|-------------|-------------|-------------|-------------|
| 051117a | 0      | 113                    | 231                   | 16,046      | 2,410,600   | ...         | ...         | ...         |
|         | 1      | 295                    | 571                   | 16,046      | 2,410,600   | ...         | ...         | ...         |
|         | 2      | 571                    | 729                   | 16,046      | 2,410,600   | ...         | ...         | ...         |
|         | 3      | 817                    | 1044                  | 16,046      | 2,410,600   | ...         | ...         | ...         |
|         | 4      | 1044                   | 1237                  | 16,046      | 2,410,600   | ...         | ...         | ...         |
|         | 5      | 1237                   | 1466                  | 16,046      | 2,410,600   | ...         | ...         | ...         |
|         | 6      | 1466                   | 1737                  | 16,046      | 2,410,600   | ...         | ...         | ...         |
| 051210. | 0      | 115                    | 152                   | ...         | ...         | ...         | 162         | 426         |
|         | 1      | 86                     | 245                   | 258         | 20,156      | ...         | ...         | ...         |
|         | 2      | 4951                   | 37,986                | ...         | ...         | ...         | ...         | ...         |
| 060109. | 0      | 4305                   | 6740                  | 8784        | 325,220     | ...         | ...         | ...         |
|         | 1      | 75                     | 137                   | 2905        | 712,320     | ...         | ...         | ...         |
|         | 2      | 145                    | 204                   | 2905        | 712,320     | ...         | ...         | ...         |
|         | 3      | 215                    | 433                   | 2905        | 712,320     | ...         | ...         | ...         |
| 060115. | 0      | 331                    | 680                   | 117         | 257         | ...         | ...         | ...         |
|         | 1      | 283                    | 644                   | 10,605      | 14,232      | 32,067      | 74,305      | ...         |
|         | 2      | 644                    | 1007                  | 10,458      | 14,432      | 33,443      | 71,248      | ...         |

**Note.—** In many cases the underlying spectra were constrained with one time region with sufficient photons to obtain spectral parameters, and thus there are no entries in the last four columns. In some cases statistics were maximized by using multiple time regions for the underlying portion. In a few instances there are dashes for all underlying time regions, indicating that the canonical value for the underlying spectral index was used, as described in the text.

2. **THE SAMPLE**

The initial sample was chosen by looking at all *Swift* XRT light curves, between launch and 2006 January 24, and eliminating the ones that did not show any hint of deviation from a power-law decay with typical breaks (see Zhang et al. 2006, Nousek et al. 2006, and O'Brien et al. 2006 for a discussion of typical light-curve breaks). The remaining light curves were then fit with a broken power-law decay (referred to as the underlying decay curve and subscripted throughout text with UL) superposed with a power-law rise and decay for any flares that appeared above this underlying decay curve. The start time of the flare was then defined as the time that the power-law rise of the flare intersected the underlying decay power law. Similarly, the stop time of the flare was then defined as the time that the power-law decay of the flare intersected the underlying decay power law. These times, $t_{\text{start}}$ and $t_{\text{stop}}$, are defined relative to the trigger time, $T_0$, of the GRB. The signal-to-noise ratio ($S/N$) of the flare was then defined, using simple Poisson statistics, as

$$
S/N = \frac{N_{\text{total}} - N_{\text{UL}}}{\sqrt{N_{\text{total}} + N_{\text{UL}}}},
$$

where $N_{\text{total}}$ is defined as the total number of photons during the flare time interval, and $N_{\text{UL}}$ is defined as the number of photons from the fit to the underlying decay curve during the flare time interval. Only the flares with $S/N > 3$ were retained in the sample. This analysis of 110 GRBs resulted in 33 GRBs with at least one significant flare, and it resulted in a total of 77 flare time intervals, which are listed in Table 1. Some of these 77 time intervals overlap one another, so it is not always clear where one flare begins and another ends. We define the start and end of each flare as described in the analysis section below. This sample and the sample of Paper I are largely overlapping, but they differ somewhat due to the different approach and goals. The flares for which temporal properties can be obtained are frequently different from those for which spectral properties can be obtained.

3. **ANALYSIS**

The data were reduced using the latest HEAsoft tools (ver. 6.1.0), including *Swift* software version 2.0, and the latest response (ver. 8) and ancillary response files (created using xrtmkarf) available in CALDB at the time of analysis. Data were screened...
Fig. 1.—Properties of absorbed power-law spectral fits to data from a region of the light curve in which no flares were present, for all GRBs with gold flares (i.e., these are the spectral parameters of the underlying light curve). The index number of the flares shown on the x-axis simply refers to the index number for each flare shown in col. (1) of Table 3.

Fig. 2.—Properties of power-law spectral fits to flare data for all gold flares. The index number of the flares shown on the x-axis simply refers to the index number for each flare shown in col. (1) of Table 3. The top panel corresponds to the fit for the neutral hydrogen column density, the second panel corresponds to the photon index ($\Gamma_{\text{fit}}$), and the bottom panel is the reduced $\chi^2$ for each fit.
with standard parameters, including the elimination of time periods when the CCD temperature was warmer than \(-48^\circ\) C. When analyzing windowed timing (WT) data, only grades 0–2 were included, and when using photon counting (PC) mode data, only grades 0–12 were included. Source and background regions were both chosen in a way that avoids overlap with serendipitous sources in the image. For PC mode data, the source region was typically a 20 pixel (47") radius circle. The background region was typically a circle with a radius of 60 pixels chosen in a source-free region (40 pixels if the field was crowded). All quoted errors are 1 \(\sigma\) unless otherwise stated.

In order to avoid pile-up effects in some of the higher count rate PC mode data (>0.5 counts s\(^{-1}\)), an annular source extraction region was used with an inner radius that varied as a function of rate. WT mode data are free of significant pile-up effects for nearly all of the flares. However, pile-up does begin to have a marginal systematic effect on WT mode data above 100 counts s\(^{-1}\). For the few flares in this sample with a brief excursion above 100 counts s\(^{-1}\), the effect of pile-up is insignificant on this analysis, since it averages the spectrum over the entire time interval of the flare, and as a result the vast majority of flare photons are not affected by pile-up.

### 3.1. Light-Curve Analysis

The light curves and the corresponding temporal analysis are presented in Paper I. However, it is worth mentioning a few of the
temporal analysis issues related to the spectral analysis presented here. In particular, there are a few differences between the approaches of this paper and Paper I. The $t_{\text{start}}$ and $t_{\text{stop}}$ times in our analysis were not constrained to be exactly the same as those of Paper I. However, they are approximately the same, and the differences are irrelevant for the purposes of fitting the spectra. The small differences arise from the fact that this analysis fits temporal power-law curves to the rise and decay portions of the flares, whereas Paper I fits Gaussians to the flares. The points on the light curve where these power laws intersect the underlying decay curve power law are defined as $t_{\text{start}}$ and $t_{\text{stop}}$, and they are reported in Table 1. This method allows us to easily define a temporal region for performing spectral fits on flare data, even if the flare is missing a large fraction of its light curve for any reason. We are still able to fit a spectrum to large flares that are missing some data on the rising or falling portion of the flare, even if they do not have a well-constrained temporal fit. When calculating the fluence in that portion of the flare, a correction factor is applied based on a power-law extrapolation of the flare light curve. To define the underlying decay curve, we use multiply broken power laws that account for the various phases of the GRB and afterglow light-curve decays (Nousek et al. 2006; Zhang et al. 2006; O’Brien et al. 2006).

In some cases the time range for spectral extraction did not include the entire flare time range due to reasons such as incomplete light curves or overlapping flares. The time regions used for spectral extraction are shown in Table 2. This table shows the times for flare spectral extraction and underlying light-curve spectral extraction. In some cases the underlying spectral extraction used multiple time regions to improve statistics. In other cases there was one large contiguous time period for underlying spectral extraction.

### 3.2. Spectral Analysis

Spectral models were fit to data using Xspec version 12.2.0 (Arnaud et al. 2005). Spectra were fit in the 0.3 to 10.0 keV energy range. A systematic error of 3% was assigned throughout the energy range due to uncertainties in the response of the instrument, particularly below 0.6 keV. During fitting, all spectra were binned to $\geq 20$ photons bin$^{-1}$, and $\chi^2$ statistics were used.

This work is attempting to apply four different models to flare spectral data. However, it is clear that the flare itself is not the only X-ray emission during the time of the flare. The underlying afterglow of the GRB is usually already in progress at the time of the flare. In some cases this is a small fraction of the flux from the flare and would merely add a small systematic effect to the spectral fit. However, in other cases the underlying light curve is a large fraction of the observed X-ray emission, and its effect must be taken into account. We choose to do this by selecting a region of the light curve before and/or after the flare and fitting the spectra in this time region to a simple absorbed power law, which has the following form:

\[
f_{\text{UL}} = C_{\text{UL}} \left( e^{-N_{\text{H,UL}} \sigma(E)} \right) \left( \frac{E}{\text{keV}} \right)^{-\Gamma_{\text{UL}}},
\]

where $N_{\text{H,UL}}$ is the neutral hydrogen column density in units of atoms cm$^{-2}$, $\sigma(E)$ is the energy-dependent photoelectric absorption cross section (Morrison & McCammon 1983), $\Gamma$ is the
spectral photon index, and $C$ is the normalization constant in units of photons cm$^{-2}$ s$^{-1}$ keV$^{-1}$. If the fit results in a value for the $N_{\text{H,L}}$ that is significantly below the Galactic $N_{\text{H}}$, then the fit is recalculated with $N_{\text{H,L}}$ set equal to the Galactic value taken from Dickey & Lockman (1990). In cases where there are not enough photons that are obviously part of the underlying light curve (i.e., independent of the flare), a canonical value of $\Gamma = 2.0$ is chosen, and the $N_{\text{H}}$ is simply tied (i.e., forced to be equal) to the hydrogen column density in the subsequent flare fitting. $N_{\text{H,L}}$ flare is integrated over that time range to obtain the expected counts from the underlying decay during the flare. This provides the scale factor by which $C_{\text{UL}}$ must be normalized.

Once the underlying spectra and flux have been estimated, as described above, these values are frozen and used as an additive part to the four spectral models for the flares. We then attempt to fit this additive model to the overall flare plus underlying afterglow spectral data. The four models we apply are a simple power law, an exponentially cut-off power law, a power law plus blackbody, and a Band function. The application of these non-power-law models, with more complex curvature, has been motivated by the similar application of models to prompt GRB emission surveys (e.g., Band et al. 1993; Ryde 2004; Kaneko et al. 2006).
et al. 2006). For all four models, we also apply photoelectric absorption, which is free to vary. To illustrate the method, the equations of two of the models are shown below.

Simple absorbed power law:

\[ f_{total} = C_{\text{are}} \left( e^{-N_{H,\text{are}} \sigma(E)} \right) \left( \frac{E}{\text{keV}} \right)^{-\Gamma_{\text{are}}} + C_{UL} \left( e^{-N_{H,UL} \sigma(E)} \right) \left( \frac{E}{\text{keV}} \right)^{-\Gamma_{UL}}; \]  

Absorbed exponentially cut off power law:

\[ f_{total} = C_{\text{flare}} \left( e^{-N_{H,\text{flare}} \sigma(E)} \right) \left( \frac{E}{\text{keV}} \right)^{-\Gamma_{\text{flare}}} e^{-E/E_{\text{flare}}} + C_{UL} \left( e^{-N_{H,UL} \sigma(E)} \right) \left( \frac{E}{\text{keV}} \right)^{-\Gamma_{UL}}. \]  

The other two models used are the thermal blackbody-plus-power-law model and the Band function model, both of which are added to the underlying afterglow power-law model in the same way as the exponential cutoff power-law model is added to the underlying model in the equations shown above. The blackbody model and the GRB Band function model (Band et al. 1993) are described by Arnaud et al. (2005). In all cases \( C_{UL}, N_{H,UL}, \Gamma_{UL} \) are frozen to the values determined using data from a region before and/or after the flare, and all flare parameters (e.g., \( C_{\text{flare}}, N_{H,\text{flare}}, \Gamma_{\text{flare}}, E_{0,\text{flare}}, E_{c,\text{flare}}, \text{and} kT_{\text{flare}} \)) are free to vary during the fitting process.

4. SPECTRAL RESULTS

The results from applying the spectral models described above are presented in this section. In order to maximize the prospects for having reasonably constrained parameters, we selected only the flares for which there were more than 15 degrees of freedom during the fitting of the power-law flare model. From this point forward in the text, we refer to these flares as gold flares.

4.1. Overall Spectral Parameters of Underlying Decay

The spectral parameters derived by fitting an absorbed power-law model to the underlying afterglow of GRBs with gold flares are shown in Figure 1. The mean of the photon index distribution is 1.9 with a standard deviation of 0.3. This is consistent with the typical photon index for GRB afterglows.

4.2. Overall Spectral Parameters of Flares

The spectral parameters derived by fitting the absorbed power-law-plus-blackbody model to the gold flares are shown in Figure 2 and Table 3. The index of each flare, shown in column (1) of each table, corresponds to the x-axis of the plots. A simple absorbed power law can provide a reasonable fit in most cases. The spectral parameters derived by fitting the absorbed Band function model to the gold flares are shown in Figure 3 and Table 4. Once again, the fit is reasonable in nearly all cases. The spectral parameters derived by fitting the absorbed exponential cutoff model to the gold flares are shown in Figure 4 and Table 5, and the spectral parameters derived by fitting the absorbed power-law-plus-blackbody model to the gold flares are shown in Figure 5 and Table 6.
It is clear that there are many cases for which a power law provides a satisfactory fit. However, it is also clear that there are many cases for which a more complex model, such as a Band function, provides a superior fit. In order to explore the distribution of the change in the quality of fit, a histogram of the $\Delta \chi^2$ between the power-law fits and the Band function fits is shown in Figure 6. This histogram shows the $\chi^2_{\text{POW}} - \chi^2_{\text{Band}}$ for the 47 gold flares. The mean degrees of freedom were 130 and 128, respectively. For comparison, we have also simulated this same $\Delta \chi^2$ for a fake distribution of power-law spectra. To do this, we simulated 1000 fake spectra that were power laws with spectral photon indices $1.9 \pm 0.3$ and the same mean degrees of freedom as the spectra in the flare sample. These spectra were then fit in the same way that we fit the spectra of the flare sample, and the $\Delta \chi^2$ was calculated. The resulting $\Delta \chi^2$ distribution from this simulation was plotted as a curve overlaid on the histogram of the real data in Figure 6.

As expected, there are many flares that can be fit equally well by both models, but some flares have a better fit using a complex model such as the Band function. The distribution is skewed to the positive values of $\Delta \chi^2$. One way to quantify this is to compare the number of GRB flares with a large $\Delta \chi^2$ for both the real data and the simulated power-law data. For the simulated power-law data, there are 5 events from 1000 with $\Delta \chi^2 > 9.0$, so one would expect 0.23 flares in the sample of 47 gold flares to have $\Delta \chi^2 > 9.0$ by chance, if the real data had been drawn.

### Table 5

| Index Number (1) | GRB (2) | Flare (3) | $N_{\text{H}}$ $(10^{22} \text{ cm}^{-2})$ | Photon Index (5) | $E_{\text{cut}}$ (keV) | $\chi^2_{\text{red}}$ (7) | Degrees of Freedom (8) |
|------------------|---------|----------|---------------------------------|-----------------|-----------------|----------------|---------------------|
| 1                | 050219  | 1        | $40.2^{+10.6}_{-10.2}$          | 2.68$^{+0.37}_{-0.68}$ | 999             | 1.12            | 37                  |
| 2                | 050502  | 1        | $8.7^{+4.5}_{-2.2}$             | $1.97^{+1.04}_{-1.4}$ | 7.2$^{+1.4}_{-1.6}$ | 1.36            | 327                 |
| 3                | 10.8$^{+3.3}_{-2.1}$ | 3        | $2.11^{+0.8}_{-0.8}$           | 999             | 0.86            | 30                  |
| 4                | 050607  | 2        | $22.5^{+4.4}_{-3.5}$            | 2.40$^{+0.38}_{-0.83}$ | 999             | 0.87            | 32                  |
| 5                | 050712  | 2        | $23.9^{+4.1}_{-3.9}$            | 2.10$^{+0.19}_{-0.18}$ | 999             | 1.60            | 56                  |
| 6                | 051227  | 2        | $20.2^{+3.8}_{-3.8}$            | 3.06$^{+0.95}_{-0.99}$ | 999             | 1.09            | 17                  |
| 7                | 050713  | 1        | $46.2^{+6.5}_{-4.6}$            | $1.82^{+0.43}_{-0.49}$ | 8.9$^{+999}_{-6.1}$ | 1.02            | 187                 |
| 8                | 050802  | 1        | 50.4$^{+13.9}_{-10.2}$          | 3.29$^{+0.65}_{-0.65}$ | 999             | 1.21            | 47                  |
| 9                | 050716  | 1        | $23.6^{+66.7}_{-23.6}$          | 1.18$^{+1.99}_{-1.95}$ | 128.0$^{+228.0}_{-228.0}$ | 0.28            | 55                  |
| 10               | 050724  | 1        | $44.7^{+3.1}_{-5.0}$            | $1.37^{+0.04}_{-0.14}$ | 8.7$^{+4.6}_{-4.6}$ | 1.03            | 329                 |
| 11               | 050726  | 2        | $48.1^{+3.9}_{-4.9}$            | 2.32$^{+0.67}_{-0.79}$ | 4.3$^{+4.3}_{-4.3}$ | 0.95            | 53                  |
| 12               | 050730  | 1        | 10.7$^{+4.3}_{-4.3}$            | $1.61^{+0.21}_{-0.21}$ | 32.2$^{+27.6}_{-27.6}$ | 1.08            | 57                  |
| 13               | 050802  | 1        | 8.4$^{+0.5}_{-0.5}$             | 6.6$^{+0.05}_{-0.05}$ | 999             | 0.94            | 186                 |
| 14               | 050803  | 5        | 58.9$^{+10.9}_{-10.9}$          | 1.91$^{+0.08}_{-0.08}$ | 999             | 0.94            | 105                 |
| 15               | 050822  | 1        | 4.0$^{+0.0}_{-0.0}$             | $0.99^{+0.02}_{-0.02}$ | 3.3$^{+0.7}_{-0.7}$ | 0.42            | 26                  |
| 16               | 050904  | 1        | 19.3$^{+4.8}_{-4.8}$            | 2.86$^{+0.26}_{-0.3}$ | 275.2$^{+999}_{-270.1}$ | 1.07            | 30                  |
| 17               | 050916  | 1        | 4.7$^{+0.3}_{-0.3}$             | $0.99^{+0.06}_{-0.06}$ | 4.1$^{+235.8}_{-21.1}$ | 0.98            | 80                  |
| 18               | 050922  | 1        | 4.7$^{+0.3}_{-0.3}$             | $0.99^{+0.06}_{-0.06}$ | 4.1$^{+235.8}_{-21.1}$ | 0.98            | 80                  |
| 19               | 051117  | 1        | 19.5$^{+18.5}_{-18.5}$          | 2.57$^{+0.12}_{-0.15}$ | 25.2$^{+999}_{-999}$ | 0.84            | 44                  |
| 20               | 060111  | 1        | 3.1$^{+0.0}_{-0.0}$             | $0.99^{+0.06}_{-0.06}$ | 4.1$^{+235.8}_{-21.1}$ | 0.98            | 80                  |
| 21               | 060124  | 1        | 17.4$^{+0.8}_{-0.8}$            | $0.99^{+0.06}_{-0.06}$ | 4.1$^{+235.8}_{-21.1}$ | 0.98            | 80                  |
| 22               | 060125  | 2        | 16.4$^{+0.5}_{-0.5}$            | $0.99^{+0.06}_{-0.06}$ | 4.1$^{+235.8}_{-21.1}$ | 0.98            | 80                  |
from a power-law distribution. For the real data, there are 9 GRB flares from the sample of 47 gold flares that have \( \Delta \chi^2 > 9.0 \). Therefore, it is unlikely that this sample was drawn from a simple power-law spectral distribution, and it is clear that Band functions sometimes provide a superior fit. However, it is worth mentioning that a power law can provide a reasonable fit to many flares.

### 4.3. Fluence of Flares

The fluence of a flare is defined as the flux of the flare, found using the spectral fits described above, integrated over the duration of the flare from \( t_{\text{start}} \) to \( t_{\text{stop}} \) in the 0.2–10 keV energy band. Table 7 shows the fluences for both the power-law and the Band function fits to the flares. Since the spectral fits provided no compelling evidence for using the thermal model or the exponential cutoff model, for the remainder of this paper we restrict ourselves to the standard spectral models used for GRB afterglows and prompt emission, namely—the simple power law and the Band function. The quoted error bars are 1\( \sigma \), and they include the error due to the uncertainty in the underlying light-curve contribution to the fluence. In some cases this latter source of error is large and dominates the error from the spectral fit itself. The calculated fluence values for all flares (not just the gold flares) have been reported, even in cases for which there are very few degrees of freedom. As a result, some of the fluence values are poorly constrained, as reflected by the error bars.

These reported fluence values do not include the contribution from the power-law component of the spectral model that was used to approximate the underlying afterglow light-curve contribution to the flare spectrum. In other words, the fluence values in column (6) of Table 7 include only the contribution from the Band function component of the spectral model fit to the flare data, excluding the frozen power-law component from the underlying component. The fluence values in column (3) of Table 7 include only the contribution from the unfrozen flare power-law component of the spectral model fit to the flare data, once again excluding the underlying component. This is an important point to stress, since most previous papers that quote a fluence for flares actually quote the entire fluence under the light curve. This practice is misleading because the underlying afterglow light curve sometimes contributes a large, and difficult to constrain, fraction of the total fluence. The reported fluence values are also corrected for effects due to incomplete light curves for some flares. For instance, if the tail end of a flare happened to be interrupted by an orbital gap or the South Atlantic Anomaly, the incomplete flare light curve would be extrapolated until it intersected with the extrapolation of the underlying light curve. In these cases the error on this extrapolation was factored into the error on the fluence.

The fluence calculations were done in the observed XRT energy band, which is 0.2–10 keV. Since the X-ray flares emit the bulk of their energy in this band, we consider this to be the most reasonable approach. This fact is supported by the Band function spectral fits that result in X-ray peak energies, and it is supported by the fact that the X-ray flares are typically weak to undetectable by higher and lower energy instruments such as BAT and UVOT. We computed the effect of extrapolating the typical flare spectrum into the higher energy band typically reported for Swift BAT bursts. The median spectral parameters for gold flares that had a reasonable spectral fit were \( \alpha = 1.06 \), \( \beta = 2.21 \), and \( E_0 = 1.02 \text{ keV} \); where these refer to the Band function lower energy photon index, higher energy photon index, and e-folding energy,

![Graph](image-url)
From these values, it was found that extending the energy range from 0.2 – 150 keV added only 1.4% to the fluence relative to the reported 0.2 – 10 keV value. This is insignificant compared to the error bars.

The overall distribution of flare fluences is shown in Figure 7 for the absorbed power-law model and the absorbed Band function model. Once again, these fluences are for just the flare component. The two distributions plotted on the right are for the 47 gold flares that have >15 degrees of freedom in the spectral fit and $\chi^2_{\text{red}} < 1.5$, while the two distributions plotted on the left include all spectral fits. Fluence derived from both power-law fits (top) and Band function fits (bottom) are shown. The mean 0.2 – 10 keV fluence (unabsorbed) of our sample of flares, derived using Band function fits, is $2.4 \times 10^{-7}$ ergs cm$^{-2}$. There is no evidence of a bimodal distribution, which might arise if flares came from multiple processes.

### 5. Flare Fluence Versus Prompt Fluence

For the purpose of comparison, the distribution of prompt emission fluences for this sample of 33 GRBs is shown in Figure 8. The mean prompt fluence is $2.4 \times 10^{-6}$ ergs cm$^{-2}$, with a standard deviation of $2.5 \times 10^{-6}$ ergs cm$^{-2}$. The flare fluence in the 0.2 – 10 keV band, where its energy peaks, is approximately a factor of 10 less than the mean fluence of the prompt GRB emission (calculated in the 15 – 150 keV band), measured by Swift BAT. However, the distributions do overlap. In at least one case

### Table 6

Properties of Blackbody plus Power-Law Spectral Fits to Gold Flares

| Index Number (1) | GRB (2) | Flare (3) | $N_{\text{phot}}$ (10$^3$ cm$^{-2}$) | Photon Index (5) | $kT$ (keV) (6) | $\chi^2_{\text{red}}$ (7) | Degrees of Freedom (8) |
|------------------|---------|----------|-----------------------------------|------------------|----------------|-----------------|----------------------|
| 1                | 050219  | 1        | 56.8 ± 5.9                        | 2.34 ± 0.75      | 0.1 ± 0.1      | 0.96            | 36                   |
| 2                | 050502  | 1        | 6.4 ± 1.3                         | 2.06 ± 0.08      | 0.3 ± 0.0      | 1.29            | 326                  |
| 3                | 050607  | 2        | 26.0 ± 7.8                        | 2.70 ± 0.88      | 1.1 ± 0.7      | 0.89            | 31                   |
| 4                | 050712  | 1        | 31.2 ± 7.6                        | 2.52 ± 0.10      | 32.4 ± 0.68    | 1.52            | 55                   |
| 5                | 050713  | 1        | 41.6 ± 11.4                       | 1.92 ± 0.34      | 0.5 ± 0.05     | 1.01            | 186                  |
| 6                | 050802  | 1        | 62.2 ± 29.3                       | 2.45 ± 0.69      | 0.7 ± 0.05     | 1.00            | 28                   |
| 7                | 050803  | 5        | 40.0 ± 32.8                       | 0.71 ± 0.46      | 0.3 ± 0.1      | 1.16            | 32                   |
| 8                | 060111  | 1        | 35.7 ± 11.1                       | 1.24 ± 0.94      | 0.7 ± 0.2      | 0.95            | 22                   |
| 9                | 060124  | 1        | 19.4 ± 9.6                        | 2.86 ± 0.30      | 0.1 ± 0.00     | 0.87            | 74                   |
| 10               | 13.6 ± 1.2 | 2        | 1.53 ± 0.05                       | 0.4 ± 0.00       | 0.89            | 298               | 354                  |
than that of the underlying afterglows. Flare power laws have a wider distribution of spectral indices than the Band function. We compare the photon index of the power-law fit to the underlying afterglow data to the power-law photon index of the flare. The idea is further strengthened by the rapid rises and decays seen in GRB 060714, which show a decrease in $E_{\text{peak}}$ as a function of the time of the flare. Butler & Kocevski (2007) has observed the same trend in his study of several bright X-ray flares.

In Figure 11 we investigate this $E_{\text{peak}}$ versus time relationship for this large sample of flares. We have plotted the values for all of the gold flares that have a known redshift. The time axis is the flare time relative to the GRB prompt $T_0$ in the burst reference frame. The results have not been scaled by the prompt GRB $E_{\text{peak}}$ or relative to one another in any way. As a result, this is merely a test of whether or not an absolute relationship exists, independent of the individual GRB or flare parameters. There is no clear overall relationship present in the data. Due to the potential for unknown scaling from burst to burst, the spectral softening apparent in individual bursts would not necessarily be apparent when an ensemble of flares from many GRBs is plotted together, as we have done in this case.

In Figure 12 we attempt to investigate the dependence of total energy release on flare time for this sample of flares. Once again, we have restricted ourselves to plotting the values for all of the gold flares that have a known redshift. The time axis is the flare time relative to the GRB prompt $T_0$ in the burst reference frame. There is no clear relationship in the data when viewing all of the flares as a single sample, as we have done here. Of course, it is still possible that such a temporal relationship exists for the flares in an individual GRB, but a scaling factor (likely to be dependent on prompt GRB parameters) would need to be applied to each GRB and the associated set of flares to see this effect when plotting flare parameters from many GRBs.

8. $E_{\text{peak}}$ versus $E_{\text{iso}}$

Although it is clear that the flares typically peak in the X-ray band, the limited bandwidth of the study presented here (0.3–10 keV) makes it difficult to constrain their peak energies well. However, this is a topic of considerable importance, since prompt GRB emission has shown evidence of an empirical relationship between the peak energy of the spectral energy distribution and the total energy in the jet, as well as the observed timescales of the jet emission (Ghirlanda et al. 2005; Amati 2006; Liang & Zhang 2006; Firmani et al. 2006; Thompson et al. 2007). So, in spite of the narrow/unconstraining bandwidth, we have attempted to explore this relationship by looking at the relationship between the Band function $E_{\text{peak}}$ and $E_{\text{iso}}$ in this band. $E_{\text{peak}}$ is the peak energy of the Band function spectrum for the flare, which corresponds to $E_{\gamma}$, where $E_{\gamma}$ is the photon energy that is obtained from a Band function spectral fit. In this work $E_{\text{iso}}$ is defined as the isotropic equivalent energy released during the GRB flare in the 0.2 keV to 10 MeV band, assuming a Band function spectrum derived in the 0.2 to 10 keV band, where the observed flare spectra typically peak. This is calculated as

$$E_{\text{iso}} = k \left( \frac{4\pi d_{\text{lum}}^2}{(1+z)} \right) (S_{\text{obs}}),$$

where $S_{\text{obs}}$ is the unabsorbed flux measured by the observer in the 0.2–10 keV band, $z$ is the redshift, $k$ is the correction factor from the observed 0.2–10 keV band to the comoving 0.2 keV to 10 MeV band, and $d_{\text{lum}}$ is the luminosity distance calculated using a flat $\Lambda$-dominated universe with $\Omega_M = 0.31$, $\Omega_{\Lambda} = 0.69$, and $H_0 = 70 \text{ km s}^{-1} \text{ Mpc}^{-1}$. The $k$-correction factor is described in detail in Bloom et al. (2001).

In Figure 13 $E_{\text{iso}}$ (obtained as above using Band function spectral fits) is shown as a function of the redshift-corrected $E_{\text{peak}}$ exclusively for gold flares that have a redshift measurement. Due to the paucity of jet break measurements, we cannot calculate $E_{\gamma}$,
| GRB (1) | Flare (2) | Fluence ($10^{-7}$ ergs cm$^{-2}$) | Power Law | $\chi^2_{\text{red}}$ (4) | Degrees of Freedom (5) | Fluence ($10^{-7}$ ergs cm$^{-2}$) | Band Function | $\chi^2_{\text{red}}$ (7) | Degrees of Freedom (8) |
|---------|-----------|-----------------------------------|-----------|--------------------------|------------------------|-----------------------------------|---------------|--------------------------|------------------------|
| 050219  | 1         | 0.70 999 00 60 00                | 1.09      | 38                       | 0.38 12 98 37          | 1.12                               | 36                      |
| 050406  | 1         | 0.21 14 06 60 00                | 1.78      | 7                        | 0.18 13 98 37          | 3.08                               | 6                       |
| 050421  | 1         | 0.21 14 06 60 00                | 0.53      | 10                       | 0.27 12 98 32          | 1.98                               | 8                       |
| 050502  | 1         | 12.99 17 14 00                | 1.41      | 328                      | 8.39 11 99 35          | 1.20                               | 326                     |
| 050607  | 1         | 0.20 999 00 70 00                | 1.21      | 8                        | 0.16 12 98 34          | 1.54                               | 6                       |
| 050712  | 1         | 1.09 999 00 70 00                | 0.83      | 31                       | 0.81 10 99 30          | 0.85                               | 29                      |
| 050724  | 1         | 0.90 14 13 00                | 1.41      | 328                      | 8.39 11 99 35          | 1.20                               | 326                     |
| 050726  | 1         | 0.20 999 00 70 00                | 0.93      | 37                       | 0.18 12 98 34          | 1.54                               | 6                       |
| 050730  | 1         | 0.07 999 00 70 00                | 0.36      | 55                       | 0.04 12 98 34          | 0.34                               | 53                      |
| 050774  | 1         | 0.81 14 13 00                | 1.05      | 330                      | 2.11 11 99 31          | 1.01                               | 328                     |
| 050776  | 1         | 0.34 86 31 00                | 0.95      | 54                       | 0.34 12 98 34          | 0.97                               | 52                      |
| 050802  | 1         | 1.29 04 00 00                | 1.23      | 22                       | 1.06 13 99 31          | 1.30                               | 20                      |
| 050803  | 1         | 0.20 999 00 70 00                | 0.97      | 30                       | 0.19 12 98 34          | 1.05                               | 29                      |
| 050820  | 1         | 0.30 999 00 70 00                | 0.79      | 13                       | 0.20 12 98 34          | 0.93                               | 11                      |
| 050822  | 1         | 2.97 999 00 70 00                | 1.10      | 14                       | 0.30 999 00            | 1.28                               | 12                      |
| 050904  | 1         | 0.10 88 16 00                | 1.34      | 13                       | 0.26 12 98 34          | 1.52                               | 11                      |
| 050908  | 1         | 1.92 999 00 70 00                | 1.18      | 36                       | 0.89 10 99 30          | 1.43                               | 36                      |
| 050915  | 1         | 0.29 14 13 00                | 1.66      | 2                        | 0.19 10 99 30          | 0.93                               | 19                      |
| 050916  | 1         | 0.10 999 00 70 00                | 1.10      | 22                       | 0.42 10 99 30          | 1.43                               | 22                      |
| 051006  | 1         | 0.34 14 14 00                | 1.18      | 36                       | 0.89 10 99 30          | 1.43                               | 22                      |
| 051016  | 1         | 0.07 999 00 70 00                | 1.44      | 4                        | 0.20 10 99 30          | 0.85                               | 13                      |
| 051117  | 1         | 0.41 999 00 70 00                | 0.84      | 16                       | 0.27 10 99 30          | 0.93                               | 14                      |
|         |           |                                   |           |                          |                       |                                   |                         |
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|         |           |                                   |           |                          |                       |                                   |                         |
|         |           |                                   |           |                          |                       |                                   |                         |

**TABLE 7**

**Fluence of Flares**
which corrects $E_{\text{iso}}$ by accounting for the jet opening angle. Thus, we cannot explore the tighter $E_{\text{peak}}$-$E_{\text{iso}}$ relationship reported for GRB prompt emission by Ghirlanda et al. (2005).

While it does seem clear that the flares involve a peak energy that is significantly lower than the more typical hundreds of keV observed for the initial GRB prompt emission, it is not clear if there is a strong relationship of this peak energy with $E_{\text{iso}}$, due to the large error bars and the limited sample. The relatively low $E_{\text{peak}}$ in the X-ray band is expected, of course, since the flares are observed as increases in the X-ray band, which are often not accompanied by measurable increases in other bands. Unfortunately, due to the size of the error bars on $E_{\text{peak}}$, it is not at all clear whether there is a relationship for the flares that is similar to the $E_{\text{peak}}$-$E_{\text{iso}}$ correlation found for the prompt GRB emission. The intriguing hint of a relationship evident in Figure 13 will be explored in the future using more flares and broader spectral coverage.

9. REDSHIFT DISTRIBUTION

This sample contains 14 GRBs that have a measured redshift. The redshift distribution is shown in Figure 14. The mean redshift for these 14 GRBs is $z = 2.6$. This value is consistent with the mean redshift of all Swift GRBs, which is between 2.5 and 2.8.

![Graphs of different X-ray flare distributions](image-url)

**Fig. 7.**—Unabsorbed 0.2–10.0 keV fluence distribution of flares. The two panels on the left are for all flares that had a convergent spectral fit. The two panels on the right are for gold flares that have $>15$ degrees of freedom in the spectral fit and $\chi^2_{\text{red}} < 1.5$. Fluence derived from both power-law fits (top) and Band function fits (bottom) are shown.
This shows that the flaring GRBs are not drawn from a significantly different redshift distribution than the overall sample of GRBs.

10. DISCUSSION AND CONCLUSIONS

Based on this sample drawn from the first 110 Swift GRBs, it is clear that significant X-ray flares are produced frequently and at late times. In this paper we have presented a detailed spectral analysis of 77 X-ray flares drawn from 33 GRBs. Some of these GRBs had many flares (we find seven significant flares in two of these GRBs, but there are probably even more temporally unresolved flares leading to observed intraflare variability), while many GRBs had only one or two flares. Each of the flares was treated as an individual event, and properties of the entire sample of flares were presented. Although several studies of individual flares have been published recently, this paper (along with Paper I) provides a systematic study of a large sample of flares. Furthermore, this paper is the first to correct for the effects of the underlying afterglow on the spectra of the flares. For the flares in which the fluence of the underlying light curve is a significant fraction of the fluence of the flare, the effect of the underlying photons on the flare spectra is significant.

Several spectral models were fit to each flare. These models included a simple absorbed power law, similar to the simple absorbed power law that typically fits the underlying afterglow light curve, as well as more complex models more akin to the spectral models that frequently provide a better description of GRB prompt emission, such as the GRB Band function (Band et al. 1993). For some flares, both simple and complex models provided a reasonable fit, while some flares had an improved fit by using a more complex model such as a Band function. It is unlikely that the complete distribution of spectra was drawn from a pure power-law distribution. Spectra with curvature, such as the Band function, could be related to the instantaneous source spectrum, but it should be noted that it could also be caused by temporal evolution of the spectrum during the flare (this work averaged the spectrum over the entire flare), since some flares have shown spectral evolution in time (Godet et al. 2007; Krimm et al. 2007). In any case, this result is similar to the results found...
for prompt emission from GRBs (Kaneko et al. 2006; Band et al. 1993), in which power laws sometimes provided a reasonable fit to prompt emission, while Band functions provided a better fit to the overall sample.

It was also found that the photon spectral indices of the flare spectrum did not always match those of the underlying spectrum, and the distributions were different from one another. In those cases this finding indicates a different population or mechanism for the production of the flare photons and the underlying afterglow light-curve photons. This result provides further evidence that flares are caused by some form of internal engine activity, particularly when evaluated in conjunction with the small $\Delta t/t$ values and further temporal analysis reported in Paper I, along with previous studies of individual bursts (Burrows et al. 2007; Chincarini et al. 2006; Falcone et al. 2006). In the context of the standard model this central engine activity would most likely involve very late internal shocks. These internal shocks could, in principle, arise from a distribution of Lorentz factors for the shells from earlier internal engine activity, but this seems unlikely due to the inefficiency of the kinetic energy conversion that would result from these weak internal shocks (Zhang 2007; Lazzati & Perna 2007). The late internal shocks are probably the result of late internal engine activity.

This sample contained 14 GRBs with a measured redshift, and the average redshift did not differ from the average redshift for all Swift GRBs, including those without flares. This implies that late flares cannot be explained merely as redshifted multipeaked emission from the initial prompt GRB. This result is also supported by individual burst analyses that are corrected for redshift, such as Cusumano et al. (2007), in which a high-redshift burst has very late flares in the burst rest frame. All of this implies that the large fluence values for flares reported in this paper (sometimes comparable to the prompt GRB) must be produced at very late times with peak energies in the X-ray band. GRB progenitor models must be capable of producing this emission within a comparable energy budget to that which was previously applied only to the prompt GRB emission. The fallback of material onto the central black hole after a stellar collapse could last for long time periods (Woosley 1993; MacFadyen et al. 2001) and lead to late internal engine activity, but the reduced luminosity of this model at late times means that it cannot explain all flares. Several models for continued activity of the central engine have been proposed (e.g., Perna et al. 2006; Fan et al. 2005; Dai et al. 2006; King et al. 2005; Proga & Zhang 2006; Katz 1997). These models, and others, must be evaluated in the context of the energy budget and the spectral parameters presented here.

This work has also attempted to explore the relationship between $E_{\text{peak}}$ and $E_{\text{iso}}$ for flares, in an effort to see if the Amati relationship (Amati 2006; Amati et al. 2002) is also present for flare events. This approach is necessarily restricted to flares for which the GRB redshifts are known and the spectra have enough counts to constrain the parameters. Unfortunately, this leads to only 18 flares (3 of which are from a short burst), and the parameters are not particularly well constrained, as shown in Figure 13. Although a relationship may exist and there is an intriguing hint of a correlation similar to that reported by Amati (2006) for GRB prompt emission, it is impossible to come to any firm conclusion due to the limited sample and large error bars. By looking at more
flares and analyzing data from more instruments over a wider energy band (thus improving the $E_{\text{peak}}$ constraint), this aspect of the flare study will be revisited in the future.

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