Development of an Array of Compound Refractive Lenses for Sub-Pixel Resolution, Large Field of View, and Time-Saving in Scanning Hard X-ray Microscopy

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Abstract: A two-dimensional array of compound refractive lenses (2D array of CRLs) designed for hard X-ray imaging with a 3.5 mm² large field of view is presented. The array of CRLs consists of 2D polymer biconcave parabolic 34 × 34 multi-lenses fabricated via deep X-ray lithography. The developed refractive multi-lens array was applied for sub-pixel resolution scanning transmission X-ray microscopy; a raster scan with only 55 × 55 steps provides a 3.5 megapixel image. The optical element was experimentally characterized at the Diamond Light Source at 34 keV. An array of point foci with a 55 µm period and an average size of ca. 2.1 µm × 3.6 µm was achieved. In comparison with the conventional scanning transmission microscopy using one CRL, sub-pixel resolution scanning transmission hard X-ray microscopy enables a large field of view and short scanning time while keeping the high spatial resolution.

Keywords: two-dimensional compound refractive lens array; deep X-ray lithography; scanning transmission X-ray microscopy; sub-pixel resolution

1. Introduction

Over the past few decades, an array of compound refractive lenses (CRLs [1–3]) for hard X-rays, also known as a Shack–Hartmann sensor (SHS), has been applied for wavefront analysis and multi-contrast imaging of weakly absorbing and porous objects with significantly reduced single exposure time due to the focusing properties of CRLs [4,5]. When a monochromatic X-ray plane wave illuminates a CRL array, an array of point foci is generated. A weakly absorbing object placed in front of or just behind the SHS leads to a displacement of the foci in the detector plane, allowing for reconstructing of a phase-contrast image. In the case of a porous object, the foci broaden, indicating scattering effects and resulting in a dark-field contrast image. Each contrast (absorption, phase, and scattering) can be reconstructed via Fourier transform or two-dimensional (2D) Gaussian fitting [6,7]. That method provides high temporal resolution and high sensitivity.

Using an array of CRLs, the local X-ray flux density is increased at the focal distance. Accordingly, the so-called single-shot X-ray multi-contrast imaging based on an array of CRLs, in combination with high frame-rate detectors, provides microsecond temporal resolution and allows for the investigation...
of dynamic processes [8]. However, the spatial resolution of this technique is equal to the distance between neighboring point foci and, consequently, to the period of the 2D array (tens of microns) [6]. The spatial resolution could be enhanced by scanning the object through a large number of point foci in combination with the super-resolution reconstruction, as was demonstrated using the 1D-line array of line focus CRLs [9]. Nevertheless, by utilizing the 1D array of CRLs, the spatial resolution is increased only in the scanning direction and limited by the X-ray line focus size (full width half maximum, FWHM). Thus, in the direction perpendicular to the scan direction it is equal to the size of a low resolution detector pixel. Consequently, the development of a 2D array of CRLs generating the point foci in the (sub-) µm range will overcome the mentioned limitations and increase the spatial resolution in both directions.

Recently, the use of 2D refractive lens arrays, fabricated either by additive manufacturing of a polymer with low radiation stability or by an embossing process of polyimide foils using a needle with paraboloid tip, were demonstrated for energies below 15 keV and for a field of view (FoV) of 1 mm$^2$ and 6.5 $\times$ 6.5 mm$^2$, which limits the scope of the samples studied [10,11]. Fabrication of 2D CRLs for higher energies by these techniques is a challenging task at the moment. Moreover, the current 2D refractive lenses include stitching/shifting errors, influencing the focusing performance (the point foci size is in the range of ten microns). The use of higher photon energies would allow for the study of optically thick objects, which are of high interest for the material sciences, for example, for characterization of cracks distribution in metallic plates and composite materials. Therefore, the target of this work was the development of X-ray CRL arrays for higher energies (from 15 keV to 100 keV), generating smaller point foci, allowing for a spatial resolution in the (sub-) µm range with a large area (>1 mm$^2$) to study relatively big samples.

We present a 2D 34 $\times$ 34 multi-lens array for sub-pixel resolution scanning transmission hard X-ray imaging (see Figure 1). This array has biconcave parabolic refracting surfaces, offers 1156 foci in a 3.5 mm$^2$ large field of view, and is made out of a radiation stable polymer. The required detector only needs large 55 µm $\times$ 55 µm pixels. Scanning the sample with steps clearly below the detector’s pixel size and slightly below the focal spot size of the individual lenslets provides a resolution in the range of the focal spot size over the entire field of view. This multi-lens array can be beneficially used for hard X-ray microscopy applications.

Figure 1. Principle of 2D X-ray multi-contrast imaging with the sample positioned in front of the detector for absorption contrast imaging. Illuminated by the X-ray beam, the 2D multi-lens array generates an array of point foci. The sample is placed in the focal plane. At each sample position, the intensity variations are recorded by a low resolution (LR) detector, which is placed as near as possible behind the sample. The physical aperture of the individual lenslets of the array matches the pixel size. Each focal point hits its corresponding pixel in the center. Sub-pixel resolution scanning transmission X-ray microscopy is achieved by raster-scanning the sample with sub-pixel sized steps through the point foci.
2. Materials and Methods

Two-Dimensional Multi-Lens Array Design and Fabrication

The design of a 2D array of CRLs, suitable for sub-pixel resolution scanning transmission hard X-ray microscopy, is presented.

A Medipix Merlin 3.0 photon-counting detector (FoV 14 mm × 14 mm, 256 × 256 pixels, 55 μm pixel size, CERN, Geneva, Switzerland) working in charge summing mode was used to fix the physical aperture of the individual CRLs [12]. In a 2D array of CRLs, the period of the focal points grid has to be equal to the pixel pitch of the detector; so, the individual CRLs physical apertures are 55 μm × 55 μm.

Deep X-ray lithography was used to fabricate such an array of CRLs [13]. This technique provides structures with parallel, smooth sidewalls with a roughness of about 20 nm [14]. It allows for producing the required parabolic shape of the refracting surfaces, sub-micrometer radii of curvature, and structure heights of up to 2.5 mm at KIT/IMT. We made an SHS of 34 × 34 single CRLs, resulting in a total entrance aperture of 1.87 mm × 1.87 mm, produced in a 2 mm high resist of type SU-8. SU-8 is an epoxy-based negative resist, which is radiation stable up to a deposited dose of at least 2 MJ/cm² [15]. The SU-8 resist (micro resist technology GmbH, Berlin) comes on a 525 μm silicon substrate. The X-ray absorber working mask was made of 20 μm gold absorbers on a 2.5 μm titanium membrane and was used to create SU-8 1D CRLs via deep X-ray lithography. The exposure dose was 19,845 mA*min/cm². After irradiation, it was post-exposure baked on the hot plate at 66 °C for 20 h. Then, unexposed resist was removed from the substrate during the development process. The developer solution was as follows: propylene glycol methyl ether acetate (PGMEA) for 2 h then rinsed in isopropanol for 30 min. After that, it was air-dried. Lithographic processes only provided 1D line focus lenses. Consequently, the substrate was cut by a diamond wafer saw, and to realize a point focus SHS, one of the line focus lenses had to be rotated 90° around the optical axis and mounted in an interdigitated way [16,17].

We characterized the array of CRLs at the Diamond Light Source beamline B16 to demonstrate its functionality at high photon energies. The array of CRLs was designed for 34 keV. At this energy, the photon flux is about 1 × 10⁹ ph/sec/mm². The vertical and horizontal focal lengths, \( f_{v,h} \), of the multi-lens array were chosen as \( f_{v,h} = 359 \) mm, a good compromise between small focus due to source demagnification, angular resolution, diffraction limit, and short focal length [18].

The number of lens elements per focusing direction is \( N = 92 \), the radius of curvature \( R_{v,h} = 15.9 \) μm, and the physical aperture \( A_{ph} = 55 \) μm, resulting in an angle between adjacent parabolas of \( \alpha = 60° \) (Figure 2). The parameters for vertically (v) and horizontally (h) focusing lens elements are identical. The size of the elliptical source of the Diamond Light Source is approximately \( s_{x,y} = 56 \) μm × 126 μm (vertical × horizontal, FWHM), the image distance is \( L_2 = 362 \) mm and the source distance is \( L_1 = 46.059 \) m.

Each lens element has two rectangular stabilization parts with \( b = 40 \) μm at the edges of each single lens array, resulting in a total lens element width of \( 34 \times 55 \) μm + \( 2 \times 40 \) μm = 1950 μm. To obtain mechanically stable lens elements, the web distance, \( w \), was chosen to be relatively large; \( w = 25 \) μm. With 50 μm air gaps, \( d \), between neighbor lens elements along the optical axis, this results in a multi-lens array with a total length of \( L_{CRL} = 22.5 \) mm calculated by:

\[
L_{CRL} = 2N_{v,h} \frac{1}{R_{v,h}} \left( \frac{A_{ph} (v,h)}{2} \right)^2 + 2N_{v,h}w + (2N_{v,h} - 1)d, \tag{1}
\]

The designed focal length, \( f_{v,h} \), of this multi-lens array is approximately [18]

\[
f_{v,h} \approx \frac{R_{v,h}}{2bN_{v,h}} + \frac{L_{CRL}}{6} \approx 359 \text{ mm}, \tag{2}
\]

using a refractive index decrement of \( \delta \approx \frac{0.000281}{(E/\text{keV})^2} \approx 2.43 \times 10^{-7} \) [19,20].
Figure 2. 2D biconcave parabolic polymer (SU-8) multi-lens array for 34 keV fabricated by deep X-ray lithography and mechanical assembly: (a) 3D model of two interdigitated planar compound refractive lenses (CRLs) on the silicon substrate (blue) with vertically focusing lens elements (red) and horizontally focusing lens elements (beige). (b) The design parameters are $A_{ph}$—physical aperture, $N_v$ and $N_h$—number of lens elements in the vertical and in a horizontal directions, respectively, $R$—radius of curvature, $d$—air gap, $\alpha$—angle between adjacent parabolas, $w$—web distance, $b$—rectangular parts at the edges for stabilizing the single lens arrays, $L_{CRL}$—total length of the multi-lens array. (c) Optical microscope image of the fabricated $34 \times 34$ multi-lens array and (d) top view.

3. Results and Discussion

3.1. X-ray Characterization of the Multi-Lens Array at B16, Diamond Light Source

The 2D multi-lens array (KIT/IMT layout number 1836 #21, lot 16–365 ao20190611a) was characterized at the B16 bending magnet test beamline of the Diamond Light Source (Didcot, United Kingdom). A channel-cut monochromator, based on a Si (311) crystal, placed 20 m from the source, was used to generate 34 keV X-rays with an energy resolution of $\Delta E/E = 10^{-4}$. Point foci were measured using a high resolution indirect detector consisting of a 5 µm thick LuAG:Eu scintillator (FEE, Idar-Oberstein, Germany) combined with 10× magnification Olympus UPlanSApo microscope objective, an Optique Peter microscope system, and a pco.4000 CCD camera with 4008 px $\times$ 2672 px (PCO AG, Kelheim, Germany), resulting in an effective pixel size of 0.9 µm $\times$ 0.9 µm in the scintillator plane. The FoV of the detector was 3.6 mm (v) $\times$ 2.4 mm (h). The 2D multi-lens array was placed on a motorized hexapod allowing for precise alignment. The focal distance was determined by scanning the detector along the optical axis with 2 mm steps; at each position, an image (Figure 3a) was recorded. The data were analyzed by fitting all foci using the 2D Gaussians method, and the full width half maximum (FWHM) was calculated in both directions for every position measured along the optical axis. In this way, the measured focal length was $f_{exp,v,h} = (362 \pm 4)$ mm, which presents a good agreement with the design value $f_{v,h} = 359$ mm. The focal spot sizes (FWHM) are shown in Figure 3c in the horizontal direction and in the vertical direction in Figure 3d. The measured vertical and horizontal size of the point foci were $(2.10 \pm 0.81)$ µm and $(3.55 \pm 0.62)$ µm, respectively. As expected, the horizontal spot size was larger than the vertical one due to the source shape.

Since the main advantage of the array of CRLs concerns the increase of the photon flux density owing to its focusing properties, we used the spectral intensity enhancement (SIE) as a parameter to quantify the photon flux. The SIE is the official definition of the formerly so-called “intensity gain” [3],

...
it is defined as the ratio of radiation power through a chosen reference area at the smallest beam dimension location with and without X-ray optics \[21\]. The reference area of 1.8 µm × 1.8 µm in the focal plane with and without the array of CRLs was used for the SIE calculation of each point foci. In this study, the average measured SIE was 16 (Figure 3b). It had a higher SIE in the middle of the array, matching the horizontal FWHM (Figure 3c). The average transmission of the 2D multi-lens array (measured via the SIE for a 55 µm × 55 µm reference area, which corresponds to the size of a single 2D subCRL) was \( T_{\text{avg}} = 66\% \).

**Figure 3.** X-ray characterization of 2D multi-lens array: (a) High resolution detector image of the 34 × 34 foci generated by the multi-lens array. (b) SIE of the 34 × 34 arrays at the focal distance, using an area of 1.8 µm × 1.8 µm \((E = 34 \text{ keV})\). SIE of the first and second sub-CRL columns was weak due to a small misalignment of one mounting frame connecting the two 1D half lenses (shadowing). Horizontal (c) and vertical (d) focal width (full width half maximum, FWHM) of the 34 × 34 multi-lens array shown as a contour plot. The ordinate states the row number of sub-CRLs and the abscissa states the column number of sub-CRLs (Si substrates to the right and bottom, corresponding to Figure 2a).

For photon energies above 80 keV nickel CRLs are used to reduce the number of lens elements and thus the total length of the CRL to make it fit onto one lithography mask \[22\]. Let us consider the manufacturing of a 2D nickel CRL array with the same parameters as those used for the SU-8 2D array of biconcave parabolic shaped CRLs described in the Materials and Methods section: \( R_{v,h} = 15.9 \text{ µm}, A_{\text{ph}} = 55 \text{ µm} \). The refractive index decrement for a nickel at 100 keV is \( \delta = 1.76 \cdot 10^{-7} \), consequently, according to Equation (2), to obtain the same focal distance of \( f_{v,h} = 359 \text{ mm} \), the number of 1D planar lenses is 63 in a vertical direction and 63 in a horizontal direction. The nickel CRLs are manufactured by deep X-ray lithography and electroplating \[23\]. In order to use the gold absorber mask developed for SU-8 CRLs in this work, we only need to reverse the tone of the resist from negative to positive, using polymethylmethacrylate (PMMA). A PMMA foil of 2 mm will be glued on to the 525 µm silicon substrate. After X-ray exposure at the KARA-Litho 2 synchrotron facility, the mask pattern will be copied into the resist layer. Then, the irradiated parts will be removed from the substrate during the development process in the GG-developer and rinsed in BDG-rinse (ethanol 60 vol% + DI water 40 vol%) and washed in distilled water. After air-drying, the nickel structures will be electroplated, and the remaining resist will be stripped to produce nickel lenses without any resist residues. The substrate will be cut, and the 1D nickel CRLs array will be arranged in the orthogonal direction as described in this work.
3.2. Application of the 2D Multi-Lens Array for 2D Sub-Pixel Resolution Scanning Transmission X-ray Imaging

The low spatial resolution of the standard non-scanning technique using an array of CRLs is determined by the distance between neighboring point foci. Scanning the sample with sub-pixel size steps overcomes this limitation. In visible light microscopy, generating a high resolution image from a set of low resolution images, which are sub-pixel shifted, is known as the pixel super-resolution (SR) technique [24]. To avoid confusion, we here use the term sub-pixel resolution instead of super-resolution, where the resolution is below the diffraction limit [25].

Two dimensional sub-pixel resolution scanning transmission X-ray imaging is a straightforward extension of the one-dimensional method described in [9] and is shown in Figure 1. The point foci with an intensity \( I_0(x, y) \) created by the 2D multi-lens array, are recorded by a Medipix Merlin 3.0 photon-counting detector. The region of interest of the Medipix detector was chosen to be \( 34 \times 34 \) pixels corresponding to the geometrical size of the 2D multi-lens array. The 2D multi-lens array is positioned in the beam and aligned parallel to the detector by rotating it around the optical axis. It is parallel when a detector pixels row switches from completely dark to fully illuminated when shifting the foci of the 2D multi-lens array over the border between pixels in the vertical direction. In the same way, a column of foci is positioned above the border between detector pixels by moving the foci of the 2D multi-lens array over the detector pixels in a horizontal direction. From that position of the array of CRLs, the foci are easily centered on the detector pixels by shifting them by half a pixel pitch in vertical and in the horizontal direction. The size of the point foci is much smaller than the pixel size \( p = 55 \, \mu m \).

Each focus must illuminate only one pixel.

The sample was positioned at 349 mm behind the entrance aperture of the array of CRLs and 12 mm in front of the detector. A Siemens star, which was fabricated at KIT/IMT using deep X-ray lithography and an electroplating technique (Figure 4a), was used as a sample. The test pattern consisted of a 1 mm thick polyimide substrate (Vespel SEK-3000, DuPont) with 110 \( \mu m \) thick gold structures on top. The polyimide substrate was nearly transparent for 34 keV X-rays (transmission ca. 96 \%), the gold structures absorbed 98\% of the X-rays. The smallest features in the test pattern had a size of 2 \( \mu m \times 4 \, \mu m \).

![Figure 4](image-url)  
**Figure 4.** (a) Scanning electron microscope image of the test pattern (gold Siemens star) used for the 34 keV sub-pixel resolution hard X-ray imaging. (b) Low resolution image acquired by the Medipix Merlin 3.0 photon-counting detector. The number of pixels is \( 34 \times 34 \) (pixel size: \( 55 \, \mu m \times 55 \, \mu m \)) and equals the size of the 2D multi-lens array. The axes correspond to the pixel number.

Sample scanning was performed using a piezo stage (Attocube ECSx5050 nanopositioner, Haar, Germany) with 1 \( \mu m \) steps within the 55 \( \mu m \) pixel size. At each sample step, one low resolution image was acquired with an exposure time of 1 s (Figure 4b). Scanning one line (vertical or horizontal) took about 5 min: 110 s exposure time for 55 low resolution images plus 55 images without a sample in the beam plus 170 s for the sample moving and overhead times. Due to beam time constraints at Diamond...
B16, we could only complete two line scans, one in the vertical and one in the horizontal direction instead of a full raster scan. All X-ray images were flat field and dark field corrected.

Sub-pixel resolution image reconstruction was performed according to:

\[ A_{SR}(Mx + m, Ly + l) = \frac{I(x, y)}{I_0(x, y)} \left( S(M \times p, L \times p) + S(m \times p, l \times p) \right), \tag{3} \]

Incident X-ray point focus intensity generated by the 2D multi-lens, \( I_0(x, y) \); intensity variation due to the absorption by the sample, \( I(x, y) \); \( m, l \) represent the step number, therefore, \( m = 1, \ldots, M \) and \( l = 1, \ldots, L \); and \( S(Mp \times p, Lp \times p) \) is the raster scanning of the sample in two directions [26].

Figure 5 shows the sub-pixel image of the Siemens star obtained from the two line scans performed. The artifact in the upper right corner in Figure 5 is the result of erroneous signals of the detector. These could not be avoided in the actual measurement as their location changed. Black pixels in between the bright lines correspond to missing values due to the sparse scanning. It should be noticed that the scanning time for a complete raster-scan would be in the range of ca. 50 min. Nevertheless, under comparable conditions, it is still much faster than the conventional single lens scanning transmission X-ray microscopy. A complete raster-scan of the sample within the area equal to the pixel size would give a complete 3.5 megapixel 2D sub-pixel resolution image with 1870 px × 1870 px.

**Figure 5.** The proof of concept of sub-pixel resolution image formation of a Siemens star, including only one horizontal and one vertical line sample scanning with the sub-pixel shift. Reconstructed 2D sub-pixel resolution image (step size: 1 µm), which is a sum of the vertical and horizontal 1D sub-pixel resolution images. A complete raster-scan of the sample with 55 × 55 lines would give a complete image, where all areas now white hatched would be white with sharply defined edges. All axes correspond to the sub-pixel number.

4. Conclusions

The two-dimensional (2D) X-ray compound refractive lens arrays, fabricated via deep X-ray lithography out of an epoxy-based radiation stable polymer, for hard X-ray imaging applications (above 15 keV) is presented. The array of CRLs has precise biconcave parabolic refractive surfaces with only 20 nm roughness, providing the smallest point foci and highest and most homogeneous SIE, compared to the existing 2D array of CRLs fabricated by other techniques. Under 34 keV monochromatic X-ray illumination at the B16 beamline at the Diamond Light Source, it generated 1156 point foci, with an average size (FWHM) of 2.10 µm × 3.55 µm, allowing for a large field of view of 3.5 mm² for X-ray imaging applications to study optically thick samples with sub-pixel resolution.
Moreover, the demand for the X-ray focusing optics for high photon energies is very high due to an exponential decrease of the spectral photon flux with increasing photon energy at bending magnet synchrotron radiation sources. The realization of a 2D array of CRLs made of nickel for the photon energies above 80 keV is feasible using the same technique and was discussed in this study. Therefore, the 2D multi-lens array is an attractive optical element for hard X-ray microscopy applications requiring large FoV and high spatial resolution at synchrotron facilities.

Author Contributions: T.M., K.I., and A.M. worked out the conceptual idea of super-resolution scanning transmission X-ray microscopy. A.O., T.M. designed and A.O. and A.L. fabricated the 2D multi-lens array. P.M. fabricated the test pattern. A.O., A.L., and J.G. performed the experiment. T.M., K.I., and A.E. developed the reconstruction algorithm and analyzed the microscopy data. A.O., J.G., and A.L. evaluated the data for the multi-lens array characterization. The manuscript was written by T.M. with support from all of the co-authors. All authors have read and agreed to the published version of the manuscript.

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