A comprehensive study on lithium-based reactive hydride composite (Li-RHC) as a reversible solid-state hydrogen storage system toward potential mobile applications†

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Reversible solid-state hydrogen storage is one of the key technologies toward pollutant-free and sustainable energy conversion. The composite system LiBH₄–MgH₂ can reversibly store hydrogen with a gravimetric capacity of 13 wt%. However, its dehydrogenation/hydrogenation kinetics is extremely sluggish (~40 h) which hinders its usage for commercial applications. In this work, the kinetics of this composite system is significantly enhanced (~96%) by adding a small amount of NbF₅. The catalytic effect of NbF₅ on the dehydrogenation/hydrogenation process of LiBH₄–MgH₂ is systematically investigated using a broad range of experimental techniques such as in situ synchrotron radiation X-ray powder diffraction (in situ SR-XPD), X-ray absorption spectroscopy (XAS), anomalous small angle X-ray scattering (ASAXS), and ultra/small-angle neutron scattering (USANS/SANS). The obtained results are utilized to develop a model that explains the catalytic function of NbF₅ in hydrogen release and uptake in the LiBH₄–MgH₂ composite system.

Introduction

The global energy demand is currently covered mainly by fossil fuels and nuclear power. By following this path, it will be a question of when these limited resources will be exhausted. Moreover, massive exploitation/consumption of these resources can lead to irreversible ecological disasters. Considering these facts, strategies and concepts for clean and sustainable energy solutions are urgently needed. A widely recognized candidate for sustainable and pollutant-free energy conversion is considered to be hydrogen. This is due to its high energy density per mass unit (33.3 kW h kg⁻¹) in comparison to natural gas (13.9 kW h kg⁻¹) and liquid fossil fuels (12.4 kW h kg⁻¹), and because its combustion product is just water: 2H₂ + O₂ → 2H₂O, using a fuel cell. By using sustainable energy sources (such as sun, wind, biomass energy, etc.) to produce hydrogen, a renewable energy circuit can be created. The main obstacles hindering hydrogen being used as an energy carrier in a wide variety of industrial applications is its low volumetric energy density (~0.003 kW h dm⁻³) and its low ignition energy (~0.02 MJ at hydrogen/air volume ratio = 29%; a spark could ignite it) in comparison to gasoline (~9 kW h dm⁻³, 0.24 ml gasoline vapor) at standard conditions. In order to enhance the volumetric energy density of gaseous hydrogen, two alternative approaches are probed so far: (1) gaseous hydrogen is pressurized up to ~700 bar at 15 °C (1.2 kW h dm⁻³), and (2) gaseous hydrogen is liquefied at cryogenic temperatures (2.4 kW h dm⁻³). Although these methods do improve the volumetric energy density of gaseous hydrogen, the safety issue remains still challenging. A more convenient alternative approach is to store hydrogen chemically in metal hydrides. This concept not only improves the volumetric energy density of the gaseous hydrogen significantly, but it also avoids the above-mentioned safety issues. Since hydrogen atoms are chemically bonded (stored) in the host metal, an energy barrier has to be overcome before hydrogen can be released. Especially, light metal hydrides are of great interest for hydrogen storage in mobile applications due to their high gravimetric- and volumetric...
energy densities. In particular, borohydrides of alkaline and alkaline earth metals show exceptionally high gravimetric hydrogen storage capacity. LiBH₄ has one of the highest volumetric energy densities (4.0 kWh dm⁻³) and one of the highest gravimetric hydrogen capacities (~13 wt%). However, its decomposition starts at temperatures above 700 K according to reaction (1), due to its thermodynamic stability (67–74 kJ mol⁻¹ H₂), that is very high relative to the reference stability window (30–50 kJ mol⁻¹ H₂) defined by the DOE.¹⁵

\[
\text{LiBH}_4 \rightarrow \text{LiH} + \text{B} + \frac{3}{2}\text{H}_2 \tag{1}
\]

A partial rehydrogenation of reaction (1) can be achieved only at temperatures above 900 K and at hydrogen pressures of ~15 MPa, which makes this complex hydride unsuitable for a possible mobile and/or stationary application. An alternative approach that avoids a dramatic degradation in hydrogen capacity and simultaneously reduces the reaction enthalpy is the concept of so-called “reactive hydride composite” (RHC). In this approach, one or more metal hydrides is added to the complex metal hydride forming a high hydrogen storage capacity composite system with a lower thermodynamic stability and enhanced reversibility. The reaction-enthalpies of various systems were altered by using the this concept. In this work, MgH₂ is used to stabilize the dehydrogenation products of LiBH₄. Indeed, the overall reaction enthalpy of the LiBH₄–MgH₂ reactive hydride composite system (Li-RHC) is reduced to 46 kJ mol⁻¹ H₂ in comparison to the respective values of each single metal hydride (LiBH₄ [67 kJ mol⁻¹ H₂], MgH₂ [75 kJ mol⁻¹ H₂]),⁷,¹⁶ according to the following reaction path:

\[
2\text{LiBH}_4 + \text{MgH}_2 \leftrightarrow 2\text{LiH} + \text{MgB}_2 + 3\text{H}_2 \tag{2}
\]

Experimentally, however, this composite system can take different reaction paths depending on the applied hydrogen backpressures and temperatures. At applied hydrogen backpressures lower than 3 bar and at temperatures about 400 °C, the system’s components decompose independently:

\[
2\text{LiBH}_4 + \text{MgH}_2 \rightarrow 2\text{LiH} + \text{Mg} + \text{B} + 4\text{H}_2 \tag{3}
\]

In this case, the overall reaction enthalpy of this composite system is not altered, and it is only partially reversible (due to its possible stable decomposition products such as amorphous boron). Though reaction (2) is thermodynamically more stable compared to reaction (3), independent decomposition of the hydrides is kinetically favored in latter case. By applying hydrogen backpressures greater than 3 bar at temperatures around 400 °C, the decomposition of LiBH₄ is thermodynamically prevented, however not that of MgH₂. Thus, after decomposition of MgH₂ to metallic magnesium, subsequently Mg reacts with LiBH₄ to form MgB₂. In this case, the dehydrogenation reaction can be described as follows:

\[
2\text{LiBH}_4 + \text{MgH}_2 \rightarrow 2\text{LiBH}_4 + \text{Mg} + \text{H}_2 \tag{4.1}
\]

\[
2\text{LiH} + \text{MgB}_2 + 3\text{H}_2 \tag{4.2}
\]

Upon the dehydrogenation reaction, an amount of roughly 11.5 wt% hydrogen is released. The first reaction step proceeds endothermic, while the second reaction step takes place exothermic, which causes a reduction in the overall reaction enthalpy of the system. Hence, the formation of MgB₂ is crucial to ensure the reversibility of Li-RHC. This is, due to a graphite-like layered structure of MgB₂, compared to the close-structure of boron [Fig. S1, ESIF]. The rehydrogenation of 2LiH + MgB₂ proceeds in one step under moderate thermodynamic conditions [50 bar H₂, 350 °C], according to reaction (5):

\[
2\text{LiH} + \text{MgB}_2 + 3\text{H}_2 \rightarrow 2\text{LiBH}_4 + \text{MgH}_2 \tag{5}
\]

Although thermodynamics and reversibility of LiBH₄ can be tuned applying the RHC concept, the de/rehydrogenation reaction kinetics of the system remains rather slow. In this work, the dehydrogenation and rehydrogenation reaction kinetics of this composite system could be significantly improved (~96%) by an addition of a small amount of NbF₅. The catalytic role of NbF₅ in enhancing the dehydrogenation/rehydrogenation reaction kinetics of Li-RHC is studied in the following in detail using advanced experimental methods such as small-angle X-ray scattering (SAXS), anomalous small-angle X-ray scattering (ASAXS), small-angle neutron scattering/ultrasmall-angle neutron scattering (SANS/USANS), in situ synchrotron radiation X-ray powder diffraction (in situ SR-XPD), and high-resolution transmission electron microscopy (HR-TEM).

**Experimental**

The raw material were purchased from Sigma-Aldrich, with degree of purity of: LiBH₄ ≥ 97.0%, MgH₂ ≥ 90.0%, and NbF₅ ≥ 98.0%, and the isotope containing materials (Li¹⁵BH₄, and ⁷Li¹⁵BH₄ with purities of ≥95%) were purchased from KAT-Chem Ltd. All samples were prepared by ball-milled in a Spex 8000 mill/shaker. The Spex 8000 mill/shaker was placed in a glove box (MB-BRAUN, Germany) under a continuously purified argon atmosphere with less than 10 ppm oxygen and moisture, respectively. The milling vial and the milling balls were made of stainless steel. The utilized ball-to-powder ratio was 10 : 1. MgH₂ was premilled for 5 h before mixing it with LiBH₄/NbF₅. Volumetric measurements were performed using the Sievert’s type apparatus Hydro Quebec, Canada, in order to study the dehydrogenation/hydrogenation properties of the composite systems and prepare cycled samples for further measurements. Coupled manometric-calorimetric desorption measurements were performed by connecting a PCT-Pro instrument (Setaram and Hy-Energy, France) with a Sensys high-pressure DSC (Setaram, HP-DSC, France). For each measurement, the mass of the samples was chosen to be about 30 mg. The measurements were performed by heating the samples from room temperature up to 500 °C at 3 °C min⁻¹ under a H₂ pressure of 4 bar. In situ SR-XPD measurements were carried out at the powder diffraction beamline D3 at the DORIS III synchrotron storage ring at DESY in Hamburg, Germany. For in situ SR-XPD measurements, samples were loaded into single-crystal sapphire tubes in a glove box filled with argon.
atmosphere. The sapphire tubes were subsequently mounted in a gas pressure cell.\textsuperscript{25} Thereafter, the cell unit was transferred into the experimental hutch, where it was mounted to a gonimeter and subsequently exposed to the synchrotron beam. The incident photon wavelength was set to 0.5 Å. A MarCCD-165 area detector was applied to collect the diffracted intensities. The diffraction intensities from the sample were collected after each 30 seconds, and the sample-to-detector distance (SDD) was kept at about 125 mm. The sample was heated up by a ceramic oven placed underneath the capillary while the sample temperature was measured by a thermocouple positioned close to the sample in the capillary and controlled via a PID regulator. The temperature and pressure parameters were set to the same values as they were chosen for the volumetric measurements. The acquired 2D-patterns were further processed to a 1D diffractogram using the Fit2D program,\textsuperscript{45} and the program Findit (ICSD-database)\textsuperscript{46} was used for phase identification. X-ray absorption spectroscopy (XAS) measurements were performed at the C-beamline at DORIS III. The ideal amount of the samples for the measurements was calculated by using the program XAFSMASS.\textsuperscript{37} Samples were mixed with dry cellulose (~50 mg) in a mortar and pressed (5 bar) into pellets of 10 mm in diameter. The pellets were placed then in an aluminum sample holder and sealed with Kapton tape (55 μm, in thickness) to avoid sample’s oxidation. Niobium was measured in its various oxidation states (metallic Nb, NbF\textsubscript{5}, and NbB\textsubscript{2}) as reference material. All measurements were recorded in transmission mode as well as in fluorescence mode at the K-edge of metallic Nb (18.99 keV). For each sample, three XAS-spectra were acquired. After removing the spikes, the spectra were aligned, calibrated, and subsequently averaged. XAS data processing and analysis were conducted by using the “IFEFFIT” software package.\textsuperscript{38} Anomalous small-angle X-ray scattering (ASAXS) measurements were performed at the beamline B1 at DORIS III (DESY in Hamburg, Germany). All measurements were carried out near the K absorption edge of niobium (18.99 keV) to characterize the Nb-containing structures in the samples upon dehydrogenation/rehydrogenation cycles. Samples were mounted in an aluminum sample holder with a circular hole (5 mm in diameter and a thickness of 0.25 mm). All samples were sealed with Kapton tape to avoid any possible oxidation. The ASAXS intensities were acquired at four different energies at two SDD (D\textsubscript{min} = 885 mm and D\textsubscript{max} = 3585 mm), respectively, to cover the maximum experimental q-range available. Here, q is the magnitude of the scattering vector defined as: q = (4πl/λ)sinθ, where λ is the incident X-ray wavelength and 2θ is the respective scattering angle. The beamline was equipped with a Pilatus 300 K detector and a Si (311) double crystal monochromator with a wavelength resolution of Δλ/λ < 10\textsuperscript{-4}. All selected energies with their corresponding anomalous dispersion factors are listed in Table 1 (the calculated dispersion values are based on the theory of Cromer & Lieberman).\textsuperscript{39} Small-Angle Neutron Scattering (SANS) measurements were performed at the SANS-1 instrument at FRM II of Heinz Maier-Leibnitz Zentrum (MLZ, Bavaria, Germany).\textsuperscript{40} The thermal neutrons were from a source with a maximum flux of 8 x 10\textsuperscript{14} n cm\textsuperscript{-2} s\textsuperscript{-1}. The incident neutron wavelength could be monochromated in the range of 3.4–30 Å by applying an array of two mechanical velocity selectors with a wavelength resolution of 10% and 6%, respectively. The SDD could be set in the range of 1.1–21 m, with a maximum q range of 0.001–2 Å\textsuperscript{-1}. For the performed experiments in this work, three sample to detector distances (1.6, 8, 20 m) and two wavelengths (6 Å for 1.6 and 8 m, 12 Å for 20 m) were applied, respectively, to cover the maximum q-range available at the high q values and to cover a reasonable q-range in the low q region in order to have a good overlapping with the USANS measurements.

The scattering intensities were measured by using a 128 \textsuperscript{3}He proportional counter detector with an area of 1000 x 1020 mm\textsuperscript{2} with a count rate of 1 MHz. Silverbehenate (AgBe) was measured at a short distance (1.6 m) to calibrate the q-axis. A water standard was measured in order to set the scattering intensities onto an absolute scale. All SANS data were processed by using BerSANS software.\textsuperscript{41} In addition to SANS measurements, USANS measurements were carried out to evaluate the larger structures present in the samples. USANS measurements were performed at the BT5-Instrument at the National Institute of Standard and Technology (NIST) in Gaithersburg (Maryland, USA).\textsuperscript{42} TEM characterization was performed on a FEI TECNAI G\textsuperscript{2} machine using 200 kV, point resolution: 0.12 nm, and a field emission gun (FEG). Dark Field imaging technique (DF) was used to distinguish different phases by their diffraction. Size measurements of the particles were performed by means of an interpolated polygon tool from iTEm software,\textsuperscript{44} and the values that took into account were those from mean diameter measurements. High-resolution transmission electron microscopy (HR-TEM) images were obtained with a magnification higher than M > 300k×. In HR-TEM images, Fast Fourier Transform (FFT) was performed by Digital Micrograph software\textsuperscript{45} to obtain the diffraction patterns. These were compared with the simulated ones obtained by JEEMS software.\textsuperscript{46} Samples for TEM were prepared by dispersing a small amount of powder in hexane and then ultrasonicated the suspension for 10 min. A drop of this suspension was deposited over a commercial copper grid for TEM coated with a Formvar support film. In this procedure, the samples were exposed to air for a short period.

### Results

The first dehydrogenation reactions of pure Li-RHC and the doped Li-RHC + 0.1NbF\textsubscript{5} sample are presented in Fig. 1, where the normalized converted fraction of desorbed hydrogen is plotted over the corresponding elapsed time in hours. The overall dehydrogenation process of the pure Li-RHC system is

| # | Energy [eV] | f | f’ |
|---|------------|---|----|
| E1 | 18 322 | -3.097 | 0.557 |
| E2 | 18 822 | -4.078 | 0.542 |
| E3 | 18 924 | -5.035 | 0.542 |
| E4 | 18 926 | -5.068 | 0.543 |
| E5 | 18 976 | -6.907 | 0.668 |
completed after approximately 45 h. This reaction proceeds in two distinct steps, which are separated by a plateau region. The first reaction step is finished after 0.75 h, followed by the plateau phase, which extends nearly up to 18 h, before the second reaction step starts. The second reaction step is completed after roughly 20 h.

The dehydrogenation reaction of the doped Li-RHC + 0.1NbF₅ composite system shows significantly improved kinetics in comparison to the pure Li-RHC system. In contrary to the dehydrogenation process of the pure Li-RHC, the plateau region is not observed in this sample. For both composite systems, the first reaction step’s kinetics is very similar and is completed roughly after 0.25 h. However, the second reaction step of the doped system is improved by a factor of ~20, relative to the pure Li-RHC system. To further investigate the influence of NbF₅ on Li-RHC, coupled manometric- and DSC measurements were carried out on the pure and on the doped Li-RHC samples, and the results are shown in Fig. 2. The desorption curves were acquired using a manometric instrument in the coupled measurements confirm the results obtained by volumetric measurements. This is further confirmed by the analysis of the onset temperatures of the different peaks evolving during dehydrogenation. Apart from the first peak, due to the polymorphic transition of Li borohydride, that takes place at identical onset temperature in the two samples (113 °C), the onset temperatures of the other peaks are lower in the doped sample in comparison to the pure Li-RHC system (see Table 2). The temperature differences between the samples’ peaks increase by moving from the second (ΔT = 21 °C) to the last (ΔT = 67 °C) one. Moreover, the dehydrogenation of the RHC is completed at 500 °C, with an induction time for the Li borohydride phase smaller than for the undoped sample. The peak with a small shoulder at lower T represents this step when the fluoride is present, instead of several less intense peaks (two visible before 500 °C in Fig. 2a). Concerning the second peak in the undoped sample, it is a sharp and single event. In the doped sample, it seems that a pre-melting takes place at lower T and an exothermic reaction occurs at the end of melting. This is coupled with a slow decrease of the sample mass, i.e. to a minor hydrogen release. The kinetics of this step is very slow. The reaction rate accelerates only when the Mg hydride dehydrogenation starts (under the 3 peak). By considering the dehydrogenation enthalpies, for MgH₂ (3rd peak), values of 61 ± 2 kJ mol⁻¹ H₂ and 58 ± 2 kJ mol⁻¹ H₂ are obtained for the undoped and doped sample, respectively, which means a slight destabilization due to the presence of NbF₅. This value is in agreement with the values obtained in other studies under similar conditions.⁴⁷, ⁴⁸ A more significant destabilization effect, however, is evident for the LiBH₄ dehydrogenation enthalpy (4th peak): at 4 bar the process is not completed for the undoped sample, while it is completed for the NbF₅ containing system (characterized by an enthalpy of 13 ± 1.5 kJ mol⁻¹ H₂). This...
value is lower than the one reported for the dehydrogenation at 3 bar of the undoped system, i.e. $20 \pm 3$ kJ mol$^{-1}$ H$_2$.\(^{47}\)

To understand the effect of NbF$_5$ on the reaction mechanism of Li-RHC, \textit{in situ} SR-XPD was applied as a function of temperature. The result of these measurements is presented in Fig. 3. For the sake of a better overview, the \textit{in situ} diffraction patterns are plotted in non-isothermal (Fig. 3a) and isothermal (Fig. 3b) conditions, respectively. Fig. 3a shows the \textit{in situ} diffraction patterns of the doped sample from room temperature up to 390 °C (isothermal temperature). Intensities of the diffracted beam are plotted (in color code) over the temperature (in °C) and 2-theta diffraction angle (in degrees). As can be seen, the initial crystalline phases of the as-milled sample consist of MgH$_2$, orthorhombic LiBH$_4$ (o-LiBH$_4$), and LiF. However, no diffraction peaks of any Nb-containing phase are detected. By raising the sample’s temperature, simultaneous narrowing and shifting of the diffraction peaks are observed toward smaller angles. The narrowing of diffraction peaks can be inferred to a higher degree of recrystallization of the high-energy ball-milled material. The shift toward lower angles is due to the thermal expansion of the crystalline unit cells. The first change in the diffraction pattern occurs at about 120 °C. This is caused by the structural phase transformation of LiBH$_4$ from orthorhombic o-LiBH$_4$ (space group Pnma)\(^9\) to hexagonal h-LiBH$_4$ (space group $P6_3/mc$),\(^{39}$ and matches with the first endothermal peak in the coupled volumetric-DSC measurement in Fig. 2b. At about 370 °C, the intensities of the Bragg-peaks of MgH$_2$ start to diminish, and those of metallic Mg start to emerge. This corresponds to the second endothermic peak of the coupled volumetric-DSC curves, which is correlated to the dehydrogenation of MgH$_2 \rightarrow$ Mg + H$_2$. Shortly after that, diffraction peaks of MgB$_2$ phase are detected. The immediate appearance of MgB$_2$ after decomposition of MgH$_2$ implies a reaction between metallic Mg and molten LiBH$_4$, which corresponds to the third DSC signal in Fig. 2b. At isothermal conditions (Fig. 3b), the diffraction intensities of metallic Mg decreases rapidly, whereas the diffraction peaks of MgB$_2$ and LiH are increasing correspondingly. This further confirms the assumption of a mutual reaction between metallic Mg and liquid LiBH$_4$ phase. However, over the entire \textit{in situ} SR-XPD measurement time, the state of niobium remains unknown. This could be due to the amorphous or/nanoscale nature of Nb containing phase/s in the Li-RHC matrix.

For obtaining detailed information about these phases, X-ray absorption spectroscopy (XAS) was applied. Because XAS method allows to detect elements in very small quantities in any environment, (in crystalline, or in an amorphous state). Hence, XAS measurements were carried out at the K-edge of niobium (18.98 keV) to determine the chemical state and the local environment of niobium in the hydride matrix at different hydrogenation cycle. Near edge structure of the XAS-spectra (XANES) was used to determine niobium’s valence state in the Li-RHC system at different hydrogenation states. Additionally, pure NbF$_5$ and NbB$_2$ samples were measured as reference samples. In Fig. 4, the first derivatives of XANES of samples and
references are presented. A comparison between the XANES spectra of the doped Li-RHC samples reveals that niobium has the same oxidation states at different hydrogenation states of the hydride matrix. On the other hand, a comparison between XANES spectra of samples and the NbB2 reference shows a great accordance in all details, which suggests an oxidation change in niobium valance from Nb5+ to Nb2+. To determine the local environment of Nb in the hydride matrix at different hydrogenation states, the EXAFS region of XAS spectra of the samples-and references (NbB2 and NbF5) were extracted and Fourier transformed (FT). The resulting radial distribution functions (RDF) are shown in Fig. 5a.

A comparison between the RDF patterns of the as-milled sample and the cycled samples shows that the local environment of Nb does not change upon dehydrogenation/hydrogenation procedure of the hydride matrix, after the milling process. Nevertheless, the width and size of the RDF amplitudes of the samples are differing at different cycling stages. However, their peak positions remain unchanged over the cycles. The RDF amplitudes of the samples increase with increasing hydrogenation cycles. This indicates that the degree of order around Nb (in the hydride matrix) is increased with increasing hydrogenation cycles of the sample. The comparison between the RDF patterns of the samples and NbF5 reference shows considerably changes in the local environment of Nb in the sample already after the ball milling process relative to NbF5 confirming the observation made by XANES.

Comparing the RDF patterns of the samples and the RDF pattern of NbB2 reference shows an excellent agreement between them in overall details. This again strongly suggests the formation of NbB2 phase in the sample after the ball-milling process which remains stable upon cycling. To further confirm this observation, ab initio calculations were carried out using FEFF6 program. Results of these calculations and experimentally observed RDF patterns of the doped sample at different hydrogenation states are shown in Fig. 5b. In the calculation, the magnitudes of the scattering amplitudes were not included for electron relaxation processes since only the phase’s existence was at the center of interest. FEFF-calculations were performed assuming NbF5 and NbB2 in crystalline state (space group C12/m1; Cryst. Sys. monoclinic (ICSD #26647)), (space group P6/mmm; Cryst. Sys. hexagonal (ICSD #30328)), respectively. As can be seen in Fig. 5b, the amplitude around 1 Å could be identified as the backscattering amplitude of fluorine. Moreover, the first- and second RDF amplitudes of the samples are well described by the backscattering amplitudes of boron and Nb, respectively. This confirms the formation of NbB2 phase in the as-milled and cycled Li-RHC + 0.1NbF5 samples. Therefore, Nb’s local environment in the hydride matrix can be identified as NbB2. Further comparison between the RAD patterns of NbB2 reference and those of the samples shows that the RAD amplitudes of the samples drop significantly with increasing distance in comparison to those of the NbB2 reference. This indicates the presence of nanosized NbB2 crystalline particles in the samples, which explains the absence of any Nb containing diffraction signals in the in situ SR-XPD patterns above. To cross-check the chemical state of Nb containing phase(s) in the doped Li-RHC, and to investigate the microstructural effects of NbF5 on the hydride matrix, HR-TEM measurements were carried out. The results of these investigations are shown in Fig. 6. HR-TEM image of doped Li-RHC sample confirms the presence of nano-sized niobium-containing particles in the Li-RHC matrix. The length of each reflection \((g_{hk0})\) could be measured using the FFT images (Fig. 6b) for these particles, and based on that, the inter-planar distances \((d_{hkl} = 1/|g_{hk0}|)\) could be calculated. The values for \(|g_{hk0}|\) were in excellent agreement with those from the JEMS simulations for NbB2, thus confirming that for each case, indeed, NbB2 particles were formed. From dark field (DF) images, particle size measurements were carried out from which a local size distribution of NbB2 particles could be extracted (Fig. 6c). According to this distribution, the mean size of NbB2 particles is about 5 nm within the range between 3 and 7 nm. Additionally, HR-TEM micrographs (in DF mode) of MgB2 particles of pure- and doped Li-RHC samples in the desorbed state were taken (Fig. 6d and e). From the micrographs, size distributions of MgB2 particles in both samples were calculated, and the results are shown in Fig. 6f and g, respectively. As can be seen, the

![Fig. 5](image_url)
particle sizes of MgB$_2$ in pure Li-RHC range from 25 up to 320 nm with an average particle size of 103 nm. In the doped Li-RHC sample, the corresponding particle sizes range from 16 nm up to 60 nm with a mean particle size of 40 nm. This clearly shows that the MgB$_2$ particles in the doped Li-RHC sample (desorbed state) are much finer compared to the corresponding sizes in the Li-RHC sample. In order to characterize the size distribution of NbB$_2$ particles in the hydride matrix in more detail, SAXS and ASAXS measurements were carried out. For SAXS measurements, samples with increasing NbF$_5$ additive content (Li-RHC + xNbF$_5$ with x being: 0, 0.01, 0.025, 0.05, 0.1) were prepared to investigate the effect of the additive on the hydride matrix. The results of SAXS measurements are shown in Fig. 7.

The y-axis represents the scattering intensities in arbitrary units, and the x-axis represents the scattering vector $q$ in the inverse space (Å$^{-1}$), where $q = (4\pi/\lambda)\sin \theta$ and $2\theta$ is the scattering angle. All SAXS measurements were carried out at the energy (18.54 keV) below the K-edge absorption energy of Nb (18.99 keV), to minimize the incoherent scattering. The SAXS curve of the sample without additive content [pure Li-RHC] exhibits a small and very broad shoulder around 1 nm$^{-1}$ (which corresponds to structures of 4–7 nm in size), but otherwise, it is featureless over the entire observed $q$-range. This indicates a highly disordered material with a lack of morphological features over the measured size range. Nevertheless, the scattering curves can be divided into two main regions, which are well described by a simple $q^{-\alpha}$ power-law (dotted lines), respectively. This suggests a fractal morphology of the samples over the observed length scale.$^{31}$ At the high $q$-region, between approximately 3 nm$^{-1}$ and 10 nm$^{-1}$, the power-law exponent is roughly $\alpha = 2$, which corresponds to the scattering from a mass fractal structure. The length scale of these structures is between 1–3 nm, which is typical for distances in the grain boundaries. In the $q$-region between 0.1 nm$^{-1}$ and 1 nm$^{-1}$, the scattering curve follows a power-law behavior with an exponent of $\alpha = 3.4$, which is typical for distances in the grain boundaries.
which can be associated with scattering from particles with rough surfaces. The size scale of these particles lies in between 5 and 60 nm and larger. The fractal regions of the scattering curve gain morphological features with increasing NbF$_5$ content in the Li-RHC sample. The very broad structure at the lower $q$ region around 0.3 nm$^{-1}$ is observed first with an increment of 1 mol% NbF$_5$ content. It becomes more prominent with increasing NbF$_5$ content, while its peak center shifts toward lower angles and the width of its amplitude become extremely broad while its magnitude becomes larger. The second structure at higher $q$-region is centered around 3 nm$^{-1}$ and becomes noticeable only after a NbF$_5$ content of 2.5 mol%, but it becomes rapidly very pronounced with further addition of NbF$_5$. In contrast to the first structure at the lower $q$ region, the second structure becomes clearly visible only after adding of 5 mol% of NbF$_5$.

This is due to the length scale of the structures in this region (1–3 nm) in comparison to structures found at the low $q$ region (5–60 nm). Since the intensity of SAXS is $\sim V^2 \sim R^d$ (where $V$ is the volume, and $R$ is the sphere’s radius). Therefore, structures with relative small sizes are well discriminated by their SAXS intensities. It should also be noted that the overall fractal character of the scattering curves in both regions remain approximately valid. Interestingly, in the lower $q$ region, the power-law decreases from 3.4 to roughly 2.9 with increasing NbF$_5$ content. This indicates an increase in surface roughness ($\sim$increase in surface area) of particles in this region with increasing NbF$_5$ content. In contrast, the power-law exponent rises in the higher $q$ region from 2.0 to approximately 2.5 with increasing NbF$_5$ content, which implies a higher degree of compactness or increasing order of structures in this region with increasing NbF$_5$ content. Although a systematic relation between NbF$_5$ content and structures formed in the SAXS curves can be recognized, no specific statement about the size distribution of Nb-containing structures can be made due to the overlapping signal between the matrix and Nb containing structures. In order to extract the scattering intensities of Nb-containing structures, ASAXS measurements were carried out. Details about the ASAXS method can be found in the referred literature. $^{32-35}$ One of the obtained results of an ASAXS measurement (Li-RHC + 0.1NbF$_5$ after the milling procedure) is exemplary shown in Fig. S2a (ESI). The peak scattering, located at around 4–5 nm$^{-1}$, belongs to the scattering of the Kapton foil, which was used to seal the samples. In the inset figure, the sample’s resonant behavior is emphasized with respect to variation in energy of the incident beam (near the K absorption edge of Nb). As the energy of the incident photons approaches the K absorption edge of the resonant atoms, the scattering intensities increase at the very high $q$ region (Porod region) considerably. This effect is caused by fluorescence and inelastic Raman scattering of the resonant atoms, which leads to an additional (energy-dependent) constant scattering. However, the contribution of this constant scattering (relative to total structural scattering) becomes significant only in the Porod-region and at energies close to the absorption edge of a scattering element. $^{36}$

Fig. S2b (ESI) shows the background-corrected ASAXS scattering curves of Fig. S2a. The shape of the scattering curves gives evidence of two structures in the sample (see inset figures). At the large $q$ values of around 4 nm$^{-1}$, the structures are rather resonant, and their estimated average size is approximately 2 nm (using the rule of thumb: $d \approx 2\pi/q$). The structures located at about 0.3 nm$^{-1}$ are less resonant in comparison to structures located at smaller $q$ values, and their average size can be estimated to be around 10 nm. In order to isolate the pure resonant scattering of NbB$_2$ structures from the total scattering, the Stuhrmann method (dispersion analysis) was applied (eqn (6)). $^{37}$

$$I(q,E) = I(qd) + 2f(E)I_{orb}(q) + [f^2(E) + f^2(E)]I_R(q)$$

Here, $I_{d}(q)$ is the non-resonant scattering contribution to the overall scattering intensity, which equals the SAXS curve observed far from any resonant absorption edges. $I_{orb}(q)$ is the off-resonant (or mixed resonant) scattering contribution of superposed intensities of, both, resonant and non-resonant scattering. Using the dispersion analysis, the pure resonant scattering contribution of NbB$_2$ structures could be isolated. In Fig. 8a, as an example, a result of this procedure is shown for the as-milled sample. As can be seen, the two structures discussed above are maintained in the pure resonant scattering curve, as well. Based on this fact, a bimodal spherical size distribution (eqn (1) and (2) in ESI†) was fitted to the pure resonant scattering curves (red line in Fig. 8a), assuming a lognormal distribution. The calculated bimodal size distributions for all samples are shown in Fig. 8b and c, respectively. As shown in Fig. 8b, the size of small NbB$_2$ particles in the as-milled sample has an average size of $\sim$1 nm, which decreases slightly in number and in size (0.8 nm) after the first desorption and remains stable. In contrast to smaller particles, the bigger particles (Fig. 8c) grow after the first desorption in number and in size from 5 nm to $\sim$6 nm and remain roughly stable over the hydrogenation cycle. The bimodal size distribution and the evolution of small and larger NbB$_2$ particles during cycling can be understood if one assumes that the NbB$_2$ particles formed.
during the milling procedure are located in the grain boundaries of the hydride matrix as loosely linked mass fractals, as was suggested by SAXS results. During the 5 hours of high-energy ball milling, some clusters are merged to larger NbB₂ nanoparticles (coarsening effect). That would explain the significantly lower number of larger NbB₂ nanoparticles in the size range of 5 nm. Over the cycling procedure, some of the smaller NbB₂ nanoparticles could migrate and agglomerate to/large particles; this can explain the decreasing amount of smaller NbB₂ nanoparticles and the aggregate of larger NbB₂ nanoparticles over the cycling procedure.

To study the structural effects of NbB₂ nanoparticles in the hydride matrix (ultra) small-angle neutron scattering (SANS/USANS), measurements were carried out. For this reason, samples with and without additive after the first dehydrogenation process were measured. To determine the composition differences between particles of pure Li-RHC and doped Li-RHC + 0.1NbF₅ systems, samples with different contrast were prepared by using lithium (⁷Li)- and boron (¹¹B) isotopes, respectively. A list of samples for these measurements is given in Table 2.

All samples were measured with SANS and USANS, respectively, in order to cover all matrix structures from the nm- to the μm-range in all samples. After calibration to absolute units, SANS and USANS curves were merged. An exemplary combined SANS/USANS result is shown in Fig. S3 (ESI). To uncover the structural features depending only on the isotope effect, all SANS/USANS scattering curves of each sample with different isotopes were fitted simultaneously. Since contrast and number density of particles are directly correlated, only the number density of particles was fitted to pronounce the effect of isotope-containing structures. By applying this procedure and assuming spherical particles, size distributions of pure and doped Li-RHC nanoparticles.

![Figure 8](image-url)  
Fig. 8 (a) Pure resonant scattering curve (blue circles) of as-milled sample and its model fit (red line), mixed resonant scattering curve (red diamonds), and the total scattering curve (black squares). Evolution of isolated bimodal size distributions of (b) small and (c) large NbB₂ particles over a hydrogenation cycle of the doped Li-RHC system.

![Figure 9](image-url)  
Fig. 9 Size distribution of (a) pure Li-RHC and (b) doped Li-RHC + 0.1NbF₅ with different isotopes after the first dehydrogenation reaction.
systems were calculated. The calculated size distributions of pure and doped hydride matrices are presented in Fig. 9a and b. Both figures are plotted in a double logarithmic scale, where the x-axis represents the radii of spheres and the y-axis the volume-weighted number density of particles. The first observation of both size distributions shows that much smaller structures are present in the doped sample compared to the pure sample. Moreover, the size distributions of pure and doped Li-RHC sample, respectively, with different isotopes vary in their number densities. This can be attributed to different scattering length densities of the respective isotopes in each sample, which allow a qualitative interpretation of specific structures present in both isotope-containing samples. Due to higher coherent scattering and lower absorption cross-section of $^7$Li and $^{11}$B, the scattering intensities, hence the number density, of coherent scattering and lower absorption cross-section of $^7$Li length densities of the respective isotopes in each sample, $^{11}$B.

Mg$_{11}$B$_2$. This indicates that structures in this size range contain magnesium boride, and LiBH$_4$, as is shown in Fig. 10. The experimental observation of nano sized Mg$_{11}$B$_2$ particles, that remains stable over the dehydrogenation cycling processes. To understand the impact of NbB$_2$ on the dehydrogenation/hydrogenation reaction mechanisms on the LiBH$_4$–MgH$_2$ composite system, kinetic models on volumetric data of the pure and doped systems are applied in order to find the rate-limiting steps for the desorption reaction of each system. Since the first desorption

Discussion

Volumetric-and calorimetric measurements have shown that the addition of NbF$_5$ to the LiBH$_4$–MgH$_2$ reactive hydride composite system enhances its dehydrogenation/rehydrogenation reaction kinetics by one order of magnitude, in comparison to its pristine state (see Fig. 1). Prior to its second dehydrogenation reaction step, the pure LiBH$_4$–MgH$_2$ composite system undergoes an extended plateau region where no reaction occurs. This plateau period, however, is not observed in the NbF$_5$ doped system. Nonetheless, the dehydrogenation processes of both systems proceed in two steps. This can be explained by the phase diagram of LiBH$_4$–MgH$_2$, MgH$_3$, and LiBH$_4$, as is shown in Fig. 10. The experimental dehydrogenation reaction of Li-RHC is also plotted as supportive information, using volumetric measurements. The phase region, in which the composite system could react in one step to form LiH–MgB$_2$, is restricted by the hatched area. In this region, the equilibrium pressure of the Li-RHC system is higher than that of both individual hydrides (LiBH$_4$ and MgH$_2$); hence, a one-step reaction is preferred. However, most of this dashed area lies in the solid phase region of LiBH$_4$, where the reaction kinetic is highly constrained by mass diffusion and low surface contact area of both single hydrides. These kinetic limitations are minimized by applying experimental conditions where LiBH$_4$ is in its liquid phase. The experimental conditions applied here lie outside the dashed area (open circles, see Fig. 10). Hence, the equilibrium pressure is lower than MgH$_2$ but higher than LiBH$_4$, which leads to a two-step reaction. Although the pure- and doped Li-RHC system follow a two-step dehydrogenation reaction, their reaction paths are very different, as shown by in situ SR-XPD measurements (see Fig. 3).

The doped Li-RHC follows a more complex reaction mechanism than the pure Li-RHC (reaction (4)). One difference is the formation of LiF in the as-milled state, which remains stable over the entire reaction path. The presence of LiF in the as-milled material also implies a reaction between NbF$_5$ and the hydride matrix. However, no trace of any Nb containing phases could be detected by in situ XPD. Using the XAS, TEM, and ASAXS method, the chemical state and the local environment were determined, which indicated the presence of nano sized NbB$_2$ particles, that remains stable over the dehydrogenation and rehydrogenation cycling processes. To understand the impact of NbB$_2$ on the dehydrogenation/hydrogenation reaction mechanisms on the LiBH$_4$–MgH$_2$ composite system, kinetic models on volumetric data of the pure and doped systems are applied in order to find the rate-limiting steps for the desorption reaction of each system.
reaction step is the same for both systems, the second dehydrogenation reaction for both systems is examined using kinetic models listed in Table S1 (ESI†). For the fitting procedure, a transformed fraction of a maximum of 0.6 was chosen to describe the growth mechanism of MgB2 phase in both systems. The results of the transformed fraction α(t) of the pure Li-RHC and the doped Li-RHC + 0.1NbF5 systems are shown in Fig. S4 (see ESI†). Kinetics of both systems are well described by using a common model. The best fit suggests a two-dimensional growth of MgB2 phase with constant interface velocity of existing nuclei. The second best fit, which converges the curve with delay and diverges roughly two hours before the final state of the system, is obtained by a three-dimensional growth of MgB2 phase with constant interface velocity. Therefore, it can be concluded that the growth mechanisms of MgB2 in both systems are very similar. Based on these results, it can be assumed that the growth process of the MgB2 phase begins in a plate-like manner and at later stages the three-dimensional growth process becomes more dominant. Although the growth mechanisms of MgB2 in the pure and in the doped system are very similar, their respective rate conversion differs considerably. Therefore, it is worth focusing on the details of the second reaction step. After the decomposition of MgH2, metallic magnesium (Mg) remains in the solid phase, which is surrounded by the liquid phase of LiBH4. Thus, a reaction between these two phases can only occur at the solid–liquid interface by the formation of small nuclei of MgB2. However, the formation of these nuclei requires a certain amount of energy, which has to be delivered by the system in order to initiate a heterogeneous nucleation and growth process of MgB2 phase. Here, the classical nucleation theory (CNT) can help to understand the underlying principles of nucleation and growth of MgB2 in this complex system as a very rough approximation. A very simple model for a heterogeneous nucleation process in CNT is given by a spherically shaped nuclei and its Gibbs free energy is:

$$\Delta G_{\text{het}} = -\frac{4\pi}{3}\Delta G_{\text{r}}r^3 + 4\pi \gamma_d r^2 \theta$$  \hspace{1cm} (7)$$

where, r represents the radius of the nucleus. \(\Delta G_{\text{r}}\) stands for the energy decrease per converted unit volume, \(\gamma_d\) represents the increased interfacial energy per converted unit area between the nucleus and the matrix, and \(S(\theta)\) is the shape factor, which describes the dependency of the “wetting” angle \(\theta\) over the nucleus. For the sake of simplicity, it can be assumed that \(S(\theta) = 1\). Then, eqn (7) (with its two contributors (solid lines)) can be plotted over the nucleus’s radius, as shown in Fig. 11.

In the beginning, the nucleus is formed by a few atoms. Consequently, there are more atoms on its surface relative to its volume. Therefore, the nucleus bulk properties are dominated by surface characteristics (~\(r^2\)) of the nucleus. At a specific nucleus size, the volume properties (~\(r^3\)) of the nucleus start to determine its bulk properties. Therefore, the Gibbs free energy undergoes a maximum point \(\Delta G_{\text{het}}^*\), where both effects are mutually balanced, and the corresponding \(r\)-value is denoted as “critical nucleus size”: \(r^*\). Therefore, nuclei formed with radii less than \(r^*\) are likely to decay, whereas nuclei with radii greater than \(r^*\) are more likely to overcome this energy barrier and remain stable with significantly higher probabilities. Consequently, the plateau phase in the pure Li-RHC system can be assigned to the nucleation period of MgB2 phase. NbB2 and MgB2 have the same hexagonal crystal structure. Furthermore, NbB2 provides two possible matching planes for the MgB2 phase to grow on, namely: MgB2 \{1011\} \parallel NbB2 \{1011\} and MgB2 \{1010\} \parallel NbB2 \{1010\} with d-mismatch values of 2.3% and 0.7%, respectively, which are well below the critical value of 6%\textsuperscript{68,69}. As was deduced from the SAXS/ASAXS results, NbB2 nanoparticles are distributed in the grain boundaries of the matrix and, therefore, NbB2 nanoparticles provide pre-existing stable nucleation centres for the formation of the MgB2 phase. This can lead to a significant reduction in the interfacial energy \(\gamma_d\) (see Fig. 11, dashed red line) and reduction in lattice strains between NbB2 and MgB2, promoting the nucleation and growth of MgB2 phase in the doped Li-RHC system. As a consequence, not only the energy barrier \(\Delta G_{\text{het}}^{\text{NbB2}}\) for building stable NbB2 nuclei can be considerably reduced but also its corresponding critical nucleus size: \(r^*_{\text{NbB2}}\) (dashed-dotted blue line in Fig. 11), in comparison to pure Li-RHC. Since the thermodynamic driving forces are approximately the same in both systems, the volume contribution can be assumed to be comparable. Also, Mg provides a possible nucleation plane for MgB2, \{0001\} || Mg \{0001\}; however, its directional misfit in the altitude \{0001\} of the hexagonal unit cell amounts up to about 48%. Taking into account that nucleation favorably does not occur on flat surfaces but along the ledges, this huge misfit (48%) would considerably increase the interfacial energy \(\gamma_d\), which in turn increases \(\Delta G_{\text{het}}^{\text{Mg}}\) and \(r^*\) hence hindering the nucleation and growth of MgB2 phase significantly. Moreover, since the formation of MgB2 nuclei is energy-consuming, the nucleation centers built in the pure Li-RHC system are scarcely and inhomogeneously distributed in the matrix compared to the doped system. This leads to a much slower reaction kinetics and larger MgB2 structures, which is observed in the pure Li-RHC system. In contrast, in the doped system abundant stable nuclei are provided (by the NbB2 nanoparticles) for nucleation and growth of MgB2. In addition, Zener pinning may also limit the growth of MgB2 structures.
in the doped system. Therefore, in the doped system much smaller MgB$_2$ structures is expected, which is indeed observed by HR-TEM measurements. This is further supported by SANS/USANS results where the overall structures are observed to be smaller in the doped system in comparison to the pure system. This in turn creates significantly larger reaction surface areas in the doped Li-RHC and noticeably shorter diffusion paths relative to the pure Li-RHC system. The following schematic patch shows the key steps of the transformation of the additive, NbF$_5$, and its role in improving the kinetic behavior of the Li-RHC:

![Schematic Patch](Image)

**Conclusions**

In this study, LiBH$_4$–MgH$_2$ (Li-RHC) composite system was investigated. The dehydrogenation process of the pure LiBH$_4$–MgH$_2$ system proceeded in two steps which were separated by an incubation period and the overall reaction was completed after roughly 45 hours. The dehydrogenation/hydrogenation kinetics of this system could significantly be enhanced by an addition of small amount of NbF$_5$. Here, the dehydrogenation process took place in reaction steps as well, however, the overall desorption reaction was completed after only 1.5 hours. Various experimental methods were applied to shed some light onto the catalytic function of NbF$_5$. X-ray absorption spectroscopy (XAS) investigation revealed that the local environment of NbF$_5$ is changed during the milling process to NbB$_2$, which remained stable upon further hydrogen desorption/absorption cycles. The results of SAXS/ASAXS investigation showed a nano-size distribution of NbB$_2$ particles in the grain boundaries of the hydride matrix which are organized as loosely bounded clusters. The model also allowed concluding that NbB$_2$ act as nucleation seeds for nucleation and growth of MgB$_2$ phase, as no incubation period was observed in the doped system. Therefore, it was concluded that the presence of NbB$_2$ nanoparticles considerably lowers the interfacial tension between the matrix and MgB$_2$ nuclei, which can lead to a smaller energy barrier for the nucleation and growth process for MgB$_2$ phase in the doped Li-RHC system. Indeed, noticeably smaller matrix structures were observed by SANS/USANS and high-resolution transmission electron microscopy (HR-TEM) measurements in the doped system in comparison to those in the pure Li-RHC system.

**Conflicts of interest**

There are no conflicts to declare.

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