Research Article

Network Anomaly Detection Based on Wavelet Analysis

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Signal processing techniques have been applied recently for analyzing and detecting network anomalies due to their potential to find novel or unknown intrusions. In this paper, we propose a new network signal modelling technique for detecting network anomalies, combining the wavelet approximation and system identification theory. In order to characterize network traffic behaviors, we present fifteen features and use them as the input signals in our system. We then evaluate our approach with the 1999 DARPA intrusion detection dataset and conduct a comprehensive analysis of the intrusions in the dataset. Evaluation results show that the approach achieves high-detection rates in terms of both attack instances and attack types. Furthermore, we conduct a full day’s evaluation in a real large-scale WiFi ISP network where five attack types are successfully detected from over 30 millions flows.

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1. Introduction

Intrusion detection has been extensively studied since the seminal report written by Anderson [1]. Traditionally, intrusion detection techniques are classified into two categories: misuse detection and anomaly detection. Misuse detection is based on the assumption that most attacks leave a set of signatures in the stream of network packets or in audit trails, and thus attacks are detectable if these signatures can be identified by analyzing the audit trails or network traffic behaviors. However, misuse detection approaches are strictly limited to the latest known attacks. How to detect new attacks or variants of known attacks is one of the biggest challenges faced by misuse detection.

To address the weakness of misuse detection, the concept of anomaly detection was formalized in the seminal report of Denning [2]. Denning assumed that security violations could be detected by inspecting abnormal system usage patterns from the audit data. As a result, most anomaly detection techniques attempt to establish normal activity profiles by computing various metrics and an intrusion is detected when the actual system behavior deviates from the normal profiles. According to the characteristics of the monitored sources, anomaly detection can be classified into host-based and network-based. Typically, a host-based anomaly detection system runs on a local monitored host and uses its log files or audit trail data as information sources. The major limitation of host-based anomaly detection is its capability to detect distributed and coordinated attacks that show patterns in the network traffic. In contrast, network-based anomaly detection aims at protecting the entire networks against intrusions by monitoring the network traffic either on designed hosts or specific sensors and thus can protect simultaneously a large number of computers running different operating systems against remote attacks such as port scans, distributed denial-of-service attacks, propagation of computer worms, which stand for a major threat to current Internet infrastructure. As a result, we restrict our focus to network anomaly detection in this paper.

According to Axelsson, the early network anomaly detection systems are self-learning, that is, they automatically formed an opinion of what the subject’s normal behavior is [3]. Such self-learning techniques include the early statistical model-based anomaly detection approaches [4–6], the AI-based approaches [7] or the biological models-based approaches [8], to name a few. Although machine learning techniques have achieved good results at detecting network anomalies so far, they are still faced with some major challenges, such as “can machine learning be secure”? [9], “behavioral non-similarity in training and testing data will totally fail leaning algorithms on anomaly detection” [10], and “limited capability for detecting previously unknown...
attacks due to large number of false alerts” [11]. Considered
as an alternative to the traditional network anomaly detection
approaches or a data preprocessing for conventional
detection approaches, recently signal processing techniques
have been successfully applied to the network anomaly
detection due to their ability in point change detection and
data transforming (e.g., using CUSUM algorithm for DDoS
detection [12]).

In this paper, we propose a new network signal modelling
technique for detecting anomalies on networks. Although
the wavelet analysis technique has been used for intrusion
detection in the recent literatures [13–27], we apply it in a
different way. In particular, the general architecture of our
approach, which is illustrated in Figure 1, consists of three
components, namely, feature analysis, normal network traffic
modeling based on wavelet approximation and prediction by
ARX(AutoRegressive with eXogenous) model, and intrusion
decision. During feature analysis, we define and generate
fifteen features to characterize the network traffic behaviors,
in which we expect that the more the number of features
is, the more accurate the traffic volume information for
the entire network will be characterized. This is different
to the current wavelet-based network anomaly detection
approaches because most of them use a limited number of features (i.e., the number of packets over a time interval) or
existing features from public intrusion detection dataset (i.e.,
41 features from KDD 1999 CUP intrusion detection dataset
[28]) as the input signals. Based on the proposed fifteen
features, normal daily traffic is then modeled and represented
by a set of wavelet approximation coefficients, which can be
predicted using an ARX model. Compared to the current
approaches (e.g., [13]) that attempt to extract different
frequency components from existing network signals, our
approach is more generic and adaptive since the ARX
model used for predicting the expected value of frequency
components is trained from network traffic data collected
on the current deployment network. The output for the
normal daily traffic model is the residual that represents
the deviation of current input signal from normal/regular
behavioral signals. Residuals are finally input to the intrusion
decision engine in which an outlier detection algorithm is
running and making intrusion decisions.

The main contribution of this work consists of: (1)
choosing fifteen network flow-based features which charac-
terize the network traffic volume information as completed
as possible; (2) based on the proposed features, modeling
the normal daily network traffic using the wavelet approx-
imation and the ARX system prediction technique; during
traffic modeling process, we apply four different wavelet
basis functions and attempt to unveil a basic question when
applying wavelet techniques for detecting network attacks,
that is “do wavelet basis functions have an important impact
on reducing the false positive rate and at the same time
keeping an acceptable detection rate”?, and (3) performing
a completed analysis for the full 1999 DARPA network traffic
dataset using our detection approach. The original 1999
DARPA intrusion detection dataset is based on the raw
TCPDUMP packet data [29]. We convert all of them into
flow-based dataset. To the best of our knowledge, this is the
first work to convert the full TCPDUMP-based 1999 DAPRA
network traffic data into flow-based dataset since the 1998
DAPRA intrusion detection dataset [30] has been converted
into connection-based dataset that is now called the 1999
KDDCUP dataset [28].

The rest of the paper is organized as follows. Section 2
introduces related work, in which we briefly summarize
existing works on applying wavelet analysis techniques
for intrusion detection. Section 3 proposes our detection
approach. In particular, we describe the fifteen flow-based
features in detail and explain the reasons for selecting them;
introduce the methodology for modeling the normal daily
traffic and present the outlier detection algorithm for intru-
sion decision. Section 4 presents the experimental evaluation
of our approach and discusses the obtained results. Section 5
makes some concluding remarks and discusses future work.

2. Related Work

The wavelet analysis technique has been widely used for
network intrusion detection recently due to its inherent
time-frequency property that allows splitting signals into
different components at several frequencies. Some examples
of typical works include literatures [13–25].

In the work of Barford et al. [13], wavelet transform is
applied for analyzing and characterizing the flow-based traf-
ic behaviors, in which NetFlow signals are split into different
components at three ranges of frequencies. In particular,
low frequency components correspond to patterns over a
long period, like several days; mid frequency components
capture daily variations in the flow data; high frequency
components consist of short term variations. The three
components are obtained through grouping corresponding
wavelet coefficients into three intervals and signals are
subsequently synthesizing from them. Based on different
frequency components, a deviation algorithm is presented
to identify anomalies by setting a threshold for the signal
composed from the wavelet coefficients at different frequency
levels. The evaluation results show that some forms of DoS
attacks and port scans are detected within mid-band and
high-band components due to their inherent anomalous
alterations generated in patterns of activity. Nevertheless,
low-frequency scans and other forms of DoS attacks do not
generate such patterns even their behaviors are obviously
anomalous.
To address some limitations of wavelet analysis-based anomaly detection, such as, scale sensitive during anomaly detection, high computation complexity of wavelet transformation. Chang et al. proposed a new network anomaly detection method based on wavelet packet transform, which can adjust the decomposition process adaptively, and thus improving the detection capability on the middle and high frequency anomalies that cannot otherwise be detected by multi-resolution analysis [14]. The evaluation results with simulated attacks show that the proposed method detects the network traffic anomaly efficiently and quickly.

Some anomaly detection system prototypes based on wavelet analysis techniques have also been developed and implemented recently, such as Waveman by Huang et al. [15] and NetViewer by Kim and Reddy [16]. The evaluation results for Waveman with part of the 1999 DARPA intrusion detection dataset and real network traffic data show that the Coiflet and Paul wavelets perform better than other wavelets in detecting most anomalies under same benchmark environment. The NetViewer is based on the idea that “by observing the traffic and correlating it to the previous normal states of traffic, it may be possible to see whether the current traffic is behaving in an anomalous manner” [16]. In their previous work [17], Kim et al. proposed a technique for traffic anomaly detection through analyzing correlation of destination IP addresses in outgoing traffic at an egress router. They hypothesize that the destination IP addresses will have a high correlation degree for a number of reasons and the changes in the correlation of outgoing addresses can be used to identify network traffic anomalies. Based on this, they apply discrete wavelet transform on the address and port number correlation data over several time scales. Any deviation from historical regular norms will alter the network administrator of the potential anomalies in the traffic.

Focusing on specific types of network attacks, wavelet analysis is used to detect DoS or DDoS attacks in [18–20]. In [18], Ramanarran presented an approach named WADeS (Wavelet-based Attack Detection Signatures) for detecting DDoS attacks. Wavelet transform is applied on traffic signals and the variance of corresponding wavelet coefficients is used to estimate the attack points. In [19], Li and Lee found that aggregated traffic has strong bursty across a wide range of time scales and based on this they applied wavelet analysis to capture complex temporal correlation across multiple time scales with very low computational complexity. The energy distribution based on wavelet analysis is then used to find DDoS attack traffic since the energy distribution variance changes always cause a spike when traffic behaviors affected by DDoS attacks while normal traffic exhibits a remarkably stationary energy distribution. In [20], Dainotti et al. presented an automated system to detect volume-based anomalies in network traffic caused by DoS attacks. The system combines the traditional approaches, such as adaptive threshold and cumulative sum, with a novel approach based on the continuous wavelet transform. Not only applied for detecting specific network anomalies directly, wavelet analysis was also widely used in network measurement from the perspectives of traffic performance analysis [21], traffic anomalies diagnosing and mining [22, 23], and traffic congestion detection [24].

3. The Proposed Approach

As illustrated in Figure 1, our approach consists of three components, namely, feature analysis, normal daily traffic modeling based on wavelet approximation and ARX, and intrusion decision. In this section, we discuss each component in detail.

3.1. Feature Analysis. The major goal of feature analysis is to select and extract robust network features that have the potential to discriminate anomalous behaviors from normal network activities. Since most current network intrusion detection systems use network flow data (e.g., netflow, sflow, ipfix) as their information sources, we focus on features in terms of flows.

The following five basic metrics are used to measure the entire network’s behavior:

FlowCount. A flow consists of a group of packets going from a specific source to a specific destination over a time period. There are various flow definitions so far, such as netflow, sflow, ipfix, to name a few. Basically, one network flow should at least include a source (consisting of source IP, source port), a destination (consisting of destination IP, destination port), IP protocol, number of bytes, number of packets. Flows are often considered as sessions between users and services. Since attacking behaviors are usually different from normal user activities, they may be detected by observing flow characteristics.

AverageFlowPacketCount. The average number of packets is in a flow over a time interval. Most attacks happen with an increased packet count. For example, distributed denial-of-service (DDoS) attacks often generate a large number of packets in a short time in order to consume the available resources quickly.

AverageFlowByteCount. The average number of bytes in a flow over a time interval. Through this metric, we can identify whether the network traffic consists of large size packets or not. Some previous denial-of-service (DoS) attacks use maximum packet size to consume the computation resources or to congest data paths, such as well known ping of death (pod) attack.

AveragePacketSize. The average number of bytes per packet is in a flow over a time interval. It describes the size of packets in more detail than the above AverageFlowByteCount feature.

FlowBehavior. The ratio of FlowCount to AveragePacketSize. It measures the anomalousness of flow behaviors. The higher the value of this ratio, the more anomalous the flows since most probing or surveillance attacks start a large number of connections with small packets in order to achieve the maximum probing performance.
Based on the above five metrics, we define a set of features to describe the traffic Information for the entire network. Let $F$ denote the feature space of network flows. We use a 15-dimensional feature vector $f \in F, \{f_i\}_{i=1,2,\ldots,15}$, given in Table 1.

Empirical observations with the 1999 DARPA network traffic flow logs (converting packet into flow logs is discussed in Section 4) show that network traffic volumes can be characterized and discriminated through these features. An example is illustrated in Figures 2 and 3. By comparing the two graphs, we see that the feature “number of flows per minute” has the potential to identify the portsweep, ipsweep, pod, apache2, dictionary attacks [29]. For more information about the results of our empirical observation see http://www.ece.uvic.ca/~wlu/wavelet.htm.

### Table 1: List of features.

| Notation of features | Description |
|----------------------|-------------|
| $f_1$                | Number of TCP flows per minute |
| $f_2$                | Number of UDP flows per minute |
| $f_3$                | Number of ICMP flows per minute |
| $f_4$                | Average number of TCP packets per flow over 1 minute |
| $f_5$                | Average number of UDP packets per flow over 1 minute |
| $f_6$                | Average number of ICMP packets per flow over 1 minute |
| $f_7$                | Average number of bytes per TCP flow over 1 minute |
| $f_8$                | Average number of bytes per UDP flow over 1 minute |
| $f_9$                | Average number of bytes per ICMP flow over 1 minute |
| $f_{10}$             | Average number of bytes per TCP packet over 1 minute |
| $f_{11}$             | Average number of bytes per UDP packet over 1 minute |
| $f_{12}$             | Average number of bytes per ICMP packet over 1 minute |
| $f_{13}$             | Ratio of number of flows to bytes per packet (TCP) over 1 minute |
| $f_{14}$             | Ratio of number of flows to bytes per packet (UDP) over 1 minute |
| $f_{15}$             | Ratio of number of flows to bytes per packet (ICMP) over 1 minute |

3.2. Normal Network Traffic Modeling with Wavelet and ARX.

In this section, we first briefly review the basic theoretical concepts on wavelet transform and system identification, and then present how to model the normal daily network traffic signals in our approach.

3.2.1. Overview of Wavelet Transform and System Identification Theory. The Fourier transform is well suited only to the study of stationary signals in which all frequencies are assumed to exist at all times and it is not sufficient to detect compact patterns. In order to address this issue, the short term Fourier transform (STFT) was proposed, in which Gabor localized the Fourier analysis by taking into account a sliding window [27]. The major limitation of STFT is that it can either give a good frequency resolution or a good time resolution (depending upon the window width). In order to have a coherence time proportional to the period, Morlet proposed Wavelet transform that can achieve good frequency resolution at low frequencies and good time resolution at high frequencies [31]. Further details about Fourier analysis, STFT analysis and Wavelet transform can be found in [32]. In this paper, we use the discrete wavelet transform (DWT) since the network signals we consider have a cutoff frequency. DWT is a multistage algorithm that uses two basis functions called wavelet function $\psi(t)$ and scaling function $\phi(t)$ to dilate and shift signals. The two functions are then applied to transform input signals into a set of approximation coefficients and detail coefficients by which the input signal $X$ can be reconstructed.

System identification deals with the problem of identifying mathematical models of dynamical systems by using observed data from the system. In a dynamical system, its output depends both on its input as well as on its previous outputs. As we have known, ARX model is widely used for system identification. Let $x(t)$ represent the regressor or predictor input and $y(t)$ denote the output generated by the system we are trying to model. Then ARX [$p, q, r$] can be represented by the following linear difference equation:

$$y(t) = \sum_{i=1}^{p} a_i y(t-i) + \sum_{i=r}^{q} b_i x(t-i) + e(t),$$

(1)

where $a_i$ and $b_j$ are the model parameters. Given an ARX model with parameters $\theta$, we have the following equation to predict the value of next output:

$$\hat{y}(t | \theta) = \sum_{i=1}^{p} a_i y(t-i) + \sum_{i=r}^{q} b_i x(t-i)$$

(2)

and the prediction error $\xi(t)$ is given by

$$\xi(t) = y(t) - \hat{y}(t | \theta).$$

(3)

The purpose for deciding a particular set of values of parameters from given parametric space is to minimize the prediction error. The least-square estimate technique is usually used to obtain the optimal value of parameters $\theta$. Further details about system identification theory can be found in [33].
3.2.2. Normal Network Traffic Modelling. Modeling the normal network traffic consists of two phases, namely, wavelet decomposition/reconstruction and generation of auto regressive model. Generally, the implementation of wavelet transform is based on filter bank or pyramidal algorithm [32]. In practical implementation, signals are passed through a low pass filter \((H)\) and a high pass filter \((G)\) at each stage. Given a signal with length \(l\), we expect to obtain a filtered signal with length \(l\). Since there are two filters in each filtering stage, the total number filtered signals are \(2^l\). In order to remove the redundancies in signals, we can down sample the low pass and high pass filtered signals by half, without any information loss. The size of data can be reduced through down sampling since we are interested only in approximations in this case. After the low level details have been filtered out, the rest of coefficients represent a high level summary of signal behaviours and thus we can use them to establish a signal profile characterizing the expected behaviors of network traffic through the day. Although there also exists some other algorithms like à trous and redundant wavelet transforms that do not down sample signals after filtering [34], we use filter banks algorithm in the normal network traffic modeling. Therefore, during the wavelet decomposition/reconstruction process, the original signals are transformed into a set of wavelet approximation coefficients that represent an approximate summary of the signal, since details have been removed during filtering.

Next, in order to estimate ARX parameters and generate ARX prediction model, we use the wavelet coefficients from one part of training data as inputs and wavelet coefficients from the other part of training data as the model fitting data. The ARX fitting process is used to estimate the optimal parameters based on least square errors. The whole procedure for modeling the normal network traffic is illustrated in Figure 4. After the prediction model for the normal network traffic is obtained, we can use it to identify anomalous signals from normal ones. When the input to the model includes only normal traffic, its output, called residuals, will be close to 0, which means the predicted value generated by the model is close to the actual input normal behaviors. Otherwise, when the input to the model includes normal traffic and anomalous traffic, the residuals will include a lot of peaks where anomalies occur. In this case, residuals are considered as a sort of mathematical transformation which tries to zeroize normal network data and amplify the anomalous data.

3.3. Outlier Detection and Intrusion Decision. According to the above section, we assume that the higher the value of residuals, the more anomalous the flow is. As a result, in
order to identify the peaks (or outliers) of residuals, we implement an outlier detection algorithm based on Gaussian Mixture Model (GMM) and make intrusion decisions based on the results of the outlier detection algorithm.

In pattern recognition, it was established that Gaussian mixture distribution could approximate any distribution up to arbitrary accuracy, as long as a sufficient number of components are used [35], and thus the unknown probability density function can be expressed as a weighted sum of Gaussian with different parameters and mixing proportions [36]. Given a random variable \( x \), its probability density function \( p(x) \) can be represented as a weighted sum of components:

\[
p(x) = \sum_{i=1}^{k} \alpha_i f_i(x; \mu_i, \nu_i),
\]

where \( k \) is the number of mixture components; \( \alpha_i (1 \leq i \leq k) \) stand for the mixing proportions, whose sum is always equal to 1. \( f_i(x; \mu_i, \nu_i) \) refers to the component density function, in which \( \mu_i \) stands for the mean of variable \( x \) and \( \nu_i \) is the variance of \( x \). The density function can be a multivariate Gaussian or a univariate Gaussian.

Expectation-Maximization (EM) algorithm has been suggested as an effective algorithm to estimate the parameters of GMM [37]. Suppose the mixture component is the univariate Gaussian, the EM algorithm for GMM can be described as follows.

1. Initialize the parameter set \( \theta^0 = \{ \alpha_i^0, \mu_i^0, \sigma_i^0 \} \).
2. **E-step:** for each data \( X \sim \{ x_n \mid n = 1, 2, \ldots, N \} \) and for each mixture component \( k \), compute the posterior probability \( p(i \mid x_n) \) by solving the following equation:

\[
p(i \mid x_n) = \frac{\alpha_i N(x_n; \mu_i, \sigma_i)}{\sum_{i=1}^{k} \alpha_i N(x_n; \mu_i, \sigma_i)},
\]

3. **M-step:** reestimate the parameters based on the posterior probabilities \( p(i \mid x_n) \):

\[
\alpha_{\text{new}} = \frac{1}{N} \sum_{n=1}^{N} p(i \mid x_n),
\]

\[
\mu_{\text{new}} = \frac{\sum_{n=1}^{N} p(i \mid x_n) x_n}{\sum_{n=1}^{N} p(i \mid x_n)},
\]

\[
\sigma_{\text{new}} = \frac{\sum_{n=1}^{N} p(i \mid x_n) (x_n - \mu_{\text{new}})^2}{\sum_{n=1}^{N} p(i \mid x_n)}.
\]

4. Go to Step 2 until the algorithm converges.

In the **E-step** (Expectation step) of the above EM algorithm, the posterior probability \( p(i \mid x_n) \) is calculated for each data \( X \sim \{ x_n \mid n = 1, 2, \ldots, N \} \) and each mixture component \( i (1 \leq i \leq k) \). In **M-step** (Maximization step), the set of parameters \( \{ \alpha_i, \mu_i, \sigma_i \} \) are re-estimated based on posterior probabilities \( p(i \mid x_n) \), which maximize the likelihood function. The EM algorithm starts with some initial random parameters and then repeatedly applies the E-step and M-step to generate better parameter estimates until the algorithm converges to a local maximum.

Our outlier detection algorithm is based on the posterior probability generated by EM algorithm. The posterior probability describes the likelihood that the data pattern approximates to a specified Gaussian component. The greater the posterior probability for a data pattern belonging to a specified Gaussian component, the higher the approximation is. As a result, data are assigned to the corresponding Gaussian components according to their posterior probabilities. However, in some cases there are some data patterns whose posterior probability of belonging to any component of GMM is very low or close to zero. These data are naturally seen as the outliers or noisy data. We illustrate the detailed outlier detection algorithm in Algorithm 1.

Thresholds \( \text{th}_1 \) and \( \text{th}_2 \) correspond to the termination conditions associated with the outlier detection algorithm: \( \text{th}_1 \) measures the absolute precision required by the algorithm and \( \text{th}_2 \) is the maximum number of iterations of our algorithm. Threshold \( \text{outlier\_thres} \) refers to the minimum mixing proportion. Once the mixing proportion corresponding to one specified Gaussian component is below \( \text{outlier\_thres} \), the posterior probability of the data pattern belonging to this Gaussian component will be set to 0.

The intrusion decision strategy is based on the outcome of outlier detection: if no outlier data are detected, the network flows are normal; otherwise, the network flows represented by this outlier is reported as the intrusion.

### 4. Performance Evaluation

We evaluate our approach with the full 1999 DARPA intrusion detection dataset. In particular, we conduct a completed analysis for network traffic provided by the dataset and identify the intrusions based on each specific day. Since most current existing network intrusion detection systems use network flow data (e.g., network, sflow, ipfix, to name a few) as their information sources, we covert all the raw TCPDUMP packet data into flow-based traffic data by using the public network traffic analysis tools (e.g., Editcap [38], Tshark [39]). To the best of our knowledge, this is the first work to convert the full 1999 DARPA...
network packet logs into network flow-based logs since the 1998 DAPRA intrusion detection dataset has been converted into connection-based dataset in 1999 (i.e., 1999 KDDCUP intrusion detection dataset).

During the evaluation, the results are summarized and analyzed in three different categories, namely, how many attack instances are detected by each feature and all features correlation, how many attack types are detected by each feature and all features correlation and how many attack instances are detected for each attack type. We do not use the traditional Receiver Operating Characteristic (ROC) curve to evaluate our approach and analyze the tradeoff between the false positive rates and detection rates because ROC curves are often misleading and incomplete [40, 41]. Compared to most, if not all, other evaluations with the 1999 DARPA dataset, our evaluation covers all types of attacks and all days’ network traffic and as a result, we consider our evaluation as a completed analysis for network traffic in the 1999 DARPA dataset. Although the 1998 and 1999 DARPA dataset are the widely used and acceptable benchmark for the intrusion detection research, they are criticized in [42, 43] due to the methodology for simulating actual network environment. As a result, we conduct an evaluation with a real network traffic dataset collected on a large-scale WiFi ISP network. Next, we will briefly introduce the 1999 DARPA/MIT Lincoln intrusion detection dataset, explain the method for converting the TCPDUMP packet logs into network flow-based logs, analyze the residuals for supporting our intrusion decision assumption in Section 3.3, and discuss the intrusion detection results we obtain.

4.1. The 1999 DARPA/MIT Lincoln Intrusion Detection Dataset. The 1999 DARPA intrusion detection dataset is one of the first standard corporuses used for evaluating intrusion detection approaches offline [29] and it includes 5 weeks of sniffed traffic (tcpdump files) from two points in a simulated network, one “inside” sniffer, between the gateway router and four “victim” machines, one “outside” sniffer between the gateway and the simulated Internet, and host-based audit data collected nightly from the four victims. We consider only the “inside” tcpdump traffic during our evaluation in this paper. The five weeks are as follows:

(i) Weeks 1 and 3: no attacks (for training anomaly detection systems). During week 1, a total of 22 hours of training data is captured on the simulation network and the network does not experience any unscheduled down time. During week 3, the network is brought down early (4:00 AM) on Day 4 (Thursday) for extended unscheduled maintenance. Traffic collection is stopped on midnight of Day 5 due to weekends.

(ii) Week 2: 43 attacks belonging to 18 labelled attack types are used for system development. During week 2, the simulation network is brought down early (3:00 AM) during Day 2 (Thursday) for extended unscheduled maintenance.

(iii) Weeks 4 and 5: 201 attacks belonging to 58 attack types (40 new) are used for evaluation. During week 4, the inside traffic for Day 2 (Tuesday) is missed. During week 5, the total 22 hours traffic data is available and there is no down-time of the network.

All the attacks in the 1999 DARPA intrusion detection dataset can be grouped into five major categories:

(1) denial-of-service (DoS): an unauthorized attempt to make a computer (network) resource unavailable to its intended users, for example, SYN Flood.

(2) Remote to local (R2L): unauthorized access from a remote machine, for example, guessing password.

(3) User to root (U2R): unauthorized access to local super-user (root) privileges, for example, various buffer overflow attacks.

(4) Surveillance or probing: unauthorized probing of a host or network to look for vulnerabilities, explore configurations, or map the network’s topology, for example, port scanning.

(5) Data compromise (data): unauthorized access or modification of data on local host or remote host.

The 1999 DARPA intrusion detection evaluation dataset has been widely used for evaluating network anomaly detection systems since it was created and extended in 1999 as a succession of the 1998 DARPA’s dataset. The original 1999 DARPA’s dataset is based on raw tcpdump log files and thus most of current evaluations are based on signatures in terms of packets. In this paper, we convert all the tcpdump log files
into flow logs over a specific time interval and then based on these flow logs we conducted a full network behavioral analysis for the dataset.

4.2. Converting 1999 DARPA ID Dataset into Flow Logs. Two existing tools (editcap, tshark) are used to convert the DARPA tcpdump files into flow logs. The raw tcpdump files we consider are the “inside” tcpdump traffic files. First, editcap is used to split the raw tcpdump file into different tcpdump files based on a specific time interval. In this case, we set the time interval as one minute in order to keep it the same as the time interval of flow data provided by most industrial standard. An example of using editcap is as follows:

```
editcap-A'1999-04-09 09:00:00' inside.tcpdump 1.pcap
```

Then, the tcpdump traffic data over the specific time interval is converted into flow logs by tshark through the following commands:

```
tshark -r 1.pcap -q -n -z conv, tcp,
tshark -r 1.pcap -q -n -z conv, udp,
tshark -r 1.pcap -q -n -z ip, icmp.
```

Finally, the format of the generated DARPA flow logs is as follows:

```
(timestamp, local src IP: src port, remote dst IP: dst port,
  incoming number of packets (remote ← local), incoming number of bytes,
  outgoing (local ← remote) number of packets, outgoing number of bytes,
  total number of packets, total number of bytes, protocol).
```

An example of one flow log of DARPA is described as:

```
920275200 135.8.60.182 : 1116
→ 172.16.114.169 : 25 47 3968 77 59310 124 63278 tcp
```

4.3. Analysis for Residuals. The purpose for analyzing the residuals is to support our assumption in Section 3.3, that is the higher the value of residuals, the more anomalous the flow is. Based on this assumption, we propose an outlier detection algorithm for residuals and the intrusion decision strategy is according to the outcome of outlier detection: if no outlier data are detected, the network flows are normal; otherwise, the network flows represented by this outlier is reported as the intrusion. As an example, we analyze the traffic data on Monday, Week 5 since it includes not only normal behaviors, but also a large number attacking activities. Figure 3 in Section 3.1 illustrates the network behaviors characterized by the feature “number of flows per minute” over one day. The following Figure 5 illustrates the network behaviors characterized by residuals over same feature “number of flows per minute.” By comparing Figures 3 and 5, we conclude that the peaks of residuals identify exactly the location where attacks happen. As illustrated in Figure 3, we know that neptune (dict) attacks happen between timestamp 500 to 600 (since the flow data is based on 1 minute time period, the timestamp 500 means the 500 minutes after the starting observing time point). From Figure 5, we see that residuals generate a peak on the exact time where the attack happens. For more information about residuals for other features see http://www.ece.uvic.ca/~wlw/wavelet.htm.

4.4. Experimental Settings and Intrusion Detection Results. We have known that the 1999 DARPA data includes 5 weeks data and we use notation “w1d1” to represent data on Monday of First Week. During the training phase, in order to generate the external regressor we create the input signal by averaging and smoothing the first 7 days of data (w1d1, w1d2, w1d3, w1d4, w1d5, w3d1, and w3d2). Based on this new generated signal we get wavelet approximation coefficients, which act as the external regressor input into the ARX model. Then, we get another test signal by averaging and smoothing the rest 3 days normal data (w3d3, w3d4 and w3d5) and use this test signal to fit the ARX model. An ARX [5 5 0] model was fitted to the data using the least squares error method and the wavelet basis function we use this evaluation is Haar wavelet. We choose Haar wavelet due to its simplicity and its aptness for our evaluation purpose. The choices of other wavelet functions and their impact on detection performance are discussed in Section 4.5. On

![Figure 5: Residuals for number of flows per minute; from left to right is Figures 5(a), 5(b), and 5(c) representing TCP, UDP, and ICMP flows, respectively.](image-url)
was obtained in the test data of Monday, Week 4, where only
instances were detected. In contrast, the lowest detection rate
5, where all attack types were detected and about 95% attack
be found in [44].

The detailed discussion about the
provide us an optimal detection results when compared to
the evaluation, we set it as 0.00001 since the value can
it has an important impact on the detection results. During
detection algorithm and its selection is very important since
refers to the minimum mixing proportion in the outlier
detection algorithm and th 6 is the maximum number of
iterations required by the algorithm. We set th 5 and th 6
as 0.0001 and 5000, respectively. The parameter outlier thres
refers to the minimum mixing proportion in the outlier
detection algorithm and its selection is very important since
it has an important impact on the detection results. During
the evaluation, we set it as 0.00001 since the value can
provide us an optimal detection results when compared to
other empirical settings. The detailed discussion about the
selection of threshold on our outlier detection algorithm can
be found in [44].

We evaluate our approach with two weeks testing (week
4 and week 5) data from the 1999 DARPA flow logs. The
evaluation results are summarized and analyzed in three
different categories, namely, how many attack instances
are detected by each feature and all features correlation,
how many attack types are detected by each feature and
all features correlation, and how many attack instances
are detected for each attack type. Table 2 explains some notations
used in our experimental evaluation.

The starting time of each attack occurs and its last
time period can be referred to [29]. Table 3 illustrates the
detection rate for each day in terms of attack types and
attack instances. We found that the highest detection rate
was obtained in the traffic data collected on Monday, Week
5, where all attack types were detected and about 95% attack
instances were detected. In contrast, the lowest detection rate
was obtained in the test data of Monday, Week 4, where only
about 30% attack instances were found and almost half of
attack types were missed.

The detection results on Monday, Week 5 are illustrated
in Tables 4, 5, and 6. The detail detection results on other
days see http://www.ece.uvic.ca/~wlu/wavelet.htm.

As we discussed before, we do not use ROC curves to
evaluate our approach. Moreover, we do not calculate the
traditional detection performance metric FPR (false positive
rate) during the evaluation. The main reason is that the
residuals of an attack behavior have an impact on the
following successive normal traffic. As a result, residuals of
an attack behavior will be mixed into the normal traffic and
identifying this kind of behaviors is blurred. Ignoring these
blurring behaviors during the evaluation will generate a large
number of false alarms. A possible solution to this issue is
that we may define an attack decaying period \( t_{\text{decay}} \) which
starts from the exact time point \( t_{\text{attack}} \) when attacks happen.
When we find an attack at \( t_{\text{attack}} \), we consider all following
traffic behaviors over \( \{ t_{\text{attack}}, t_{\text{attack}} + t_{\text{decay}} \} \) as intrusions.

4.5. Comparative Studies on Four Typical Wavelet Basis Func-
tions. In this Section, we conduct a comprehensive com-
parison for four different typical wavelet basis functions on
detecting network intrusions, namely, Daubechies1 (Haar),
Coiflets1 and Symlets2 and Discrete Meyer. We attempt
to unveil and answer a question when applying wavelet
techniques for detecting network attacks, that is “can wavelet
basis functions really have an important impact on the intru-
sion detection performance?”, which can help us improving
the approach’s performance in term of reducing false positive
rate and increasing the detection rate. The evaluation is based


| Notation          | Description                                                                 |
|-------------------|-----------------------------------------------------------------------------|
| WxWdxY            | The specific date, for example, \( x = 4, y = 1 \) and W4D1 means Monday on Week 4 |
| Attack type       | Types of attacks named by DARPA/MIT Lincoln, for example, pod means ping of death attack |
| Attacking instance| Flow data collected during the period of an attack over a time interval       |
| Total number of instances | Number of sequence value of features, for example, 1 hour includes 60 instances due to 1 min time interval |
| Total number of attacking instances | Number of sequence value of features extracted from flow data with attacks, for example, an attack lasts 30 minutes and there are 30 attacking instances |
| Total number of normal instances | Number of sequence value of features extracted from pure flow data without any attack or residual of attacks |
| Total alarms      | Number of alerts generated by our approach                                  |
| Correctly detected alarms | Number of alerts that detect attacks correctly                             |
| Number of false alarms | Number of alerts that report attacks falsely, that also means the alerts report normal instances as attacks |
| Detection rate    | Ratio of correctly detected alarms to total number of attacking instances  |
| All features correlatioN | Delete the overlap of alarms generated by all 15 features                  |

Table 3: Detection rate for each day.

| Days  | W4D1 | W4D3 | W4D4 | W4D5 | W5D1 | W5D2 | W5D3 | W5D4 | W5D5 |
|-------|------|------|------|------|------|------|------|------|------|
| DR for attack types (%) | 57.14 | 94.44 | 66.67 | 84.62 | 100  | 75.0 | 71.43 | 88.89 | 74.1 |
| DR for attack instances (%) | 29.23 | 97.12 | 51.19 | 79.37 | 94.67 | 66.1 | 49.52 | 74.33 | 26.7 |
on the 1999 DARPA flow logs on Monday, Week5, in which twenty attack types occur. During the evaluation, we found that the wavelet basis function is sensitive to features. That is one basis function operating well on one feature might have bad results for the other features. For example, Coiflets1 is better than Symlets2 in terms of $f_i$, but worse than it in terms of $f_{13}$. In order to achieve an optimal solution, we have to use different wavelet basis functions for different features. Table 7 illustrates the number of attack instances detected for each attack type by different wavelet basis functions. Since attacks always last couple of minutes in DARPA, we consider all traffic appeared over the attacking period are anomalous behaviors. Thus, even only one attack instance is identified during the attacking period, we still can say the approach identify this attack type successfully. According to Table 7, all attack types are detected by Daubechies1 (Haar), 18 attack types are detected by Coiflets1 and Symlets2 over total 20 attack types that day, and 17 attack types are detected by Discrete Meyer. Generally speaking, we conclude that Daubechies1 (Haar) basis function achieves the slightly better performance than other three wavelet families.

4.6. Evaluation with Network Flows on a WiFi ISP Network. Our approach is also evaluated with three full days’ traffic on Fred-eZone, a free wireless fidelity (WiFi) network service provider operated by the City of Fredericton [45], considering the limitations of the 1999 DARPA intrusion detection dataset. Table 8 lists the general workload dimensions for the Fred-eZone network capacity. From Table 8, we see, for example, that the unique number of source IP addresses appeared over one day is about 1,055 thousands and the total of packets is about 944 millions. Three full days’ network flows are collected on Fred-eZone and we use, for example, the notation “Fred-Day1” to represent the traffic for the first day. During the training phase, in order to generate the external regressor we use the Fred-Day1 traffic as input signal. Based on this we get wavelet approximation coefficients, which act as the external regressor input into the ARX model. Then, we apply the Fred-Day2 traffic as test signal and use this test signal to fit the ARX model. The parameter settings of ARX model and the selection of the wavelet basis function are totally the same with the evaluation with the 1999 DARPA intrusion detection dataset. The traffic on Fred-Day1 and Fred-Day2 are normal since we delete all malicious network flows identified by the IDS deployed on Fred-eZone, while the traffic on Fred-Day3 is a mixture of normal and malicious network flows. In particular, six types of attacks are included on the Fred-Day3 traffic, namely, UDP_DoS, Multihost_Attack, Stealthy.Scan, Potential.Scan, HostScans and Remote_Access_Violation. Table 9 lists the number of flows, number of bytes and number of packets for each type of attack identified on that day.

During the evaluation, we use ten features as the network signals, including $f_1, f_2, f_4, f_5, f_7, f_8, f_{10}, f_{11}, f_{13}, \text{and } f_{14}$ and we do not consider the features $f_3, f_6, f_9, f_{12}$, and $f_{15}$ because they are ICMP based. From Table 9, we see that all the attacking traffic is UDP or TCP based. Similarly, Tables 10 to 12 list the evaluation results in terms of number of attack instances detected for each attack type, number of attack types detected for each feature, number of attack instances detected for each feature and all features correlation. Table 10 illustrates that our approach successfully detect five attacks over the total six attacks and the attack Potential.Scan is missed. Table 11 shows that the UDP-based features $f_1$ and $f_8$ successfully detect the UDP_DoS attack and the TCP-based features are also sensitive to the TCP-based attacks, for example, Remote_Access_Violation. The number of false alarms for our approach running with the full day’s traffic is 0, showing that the normal/daily network traffic is modeled accurately and any deviation (anomaly) on the network will lead to a large peak value compared to other points, thus easily identified by the outlier detection algorithm. As an example, Figure 6 illustrates the residuals for the feature “number of packets per flow.” For the residuals for other features generated by our model see http://www.ece.uvic.ca/~wlu/wavelet.htm.

4.7. Comparison with Existing Anomaly Detection Approaches. Many approaches have been proposed and implemented for network anomaly detection recently, most of them belong to the category of machine learning techniques or signal processing techniques. Conducting a fair comparison among all these approaches is very difficult and has not been fully done yet on the current research community to the best of our knowledge. The 1998 DAPRA and 199 DARPA intrusion detection dataset provide a raw TCPDUMP packets dataset

| Attack Type       | Number of attack instances for each attack type | Detected number of attack instances for each attack type |
|-------------------|-----------------------------------------------|------------------------------------------------------|
| apache2-dos       | 30                                            | 29                                                   |
| arppoison-probe   | 15                                            | 15                                                   |
| dict-r2l          | 17                                            | 17                                                   |
| dosnuke-dos       | 2                                             | 2                                                    |
| ffbconfig-u2r     | 10                                            | 8                                                    |
| guesttelnet-r2l   | 4                                             | 4                                                    |
| imap-r2l          | 1                                             | 1                                                    |
| ipsweep-probe     | 26                                            | 26                                                   |
| loadmodule-u2r    | 5                                             | 5                                                    |
| ls-probe          | 2                                             | 2                                                    |
| ncfp-r2l          | 2                                             | 2                                                    |
| neutron-dos       | 5                                             | 5                                                    |
| pod-dos           | 3                                             | 3                                                    |
| portsweep-probe   | 4                                             | 2                                                    |
| selfping-dos      | 2                                             | 2                                                    |
| smurf-dos         | 2                                             | 2                                                    |
| syslogd-dos       | 1                                             | 1                                                    |
| udpstorm-dos      | 16                                            | 16                                                   |
| warezclient-dos   | 2                                             | 1                                                    |
| crashis-dos       | 1                                             | 1                                                    |
Table 5: Number of attack types detected for each feature for WSD1.

| Feature | WSD1 Detected attack types |
|---------|-----------------------------|
| \( f_1 \) | apache2-dos, guessstelnet-r2l, fbconfig-u2r, pod-dos, ipsweep-probe, neutron-dos, crashiis-dos |
| \( f_2 \) | warezclient-dos, dosnuke-dos, arppoison-probe, pod-dos, ipsweep-probe |
| \( f_3 \) | smurf-dos, portsweep-probe, apache2-dos, fbconfig-u2r, arppoison-probe, ipsweep-probe, dict-r2l, udpstorm-dos |
| \( f_4 \) | loadmodule-u2r, udpstorm-dos |
| \( f_5 \) | udpstorm-dos, selfping-dos, ncftp-r2l |
| \( f_6 \) | smurf-dos, guesstelnet-r2l, loadmodule-u2r, fbconfig-u2r, arppoison-probe, ipsweep-probe, dict-r2l, syslogd-dos, neutron-dos, ls-probe, dosnuke-dos, udpstorm-dos, selfping-dos |
| \( f_7 \) | apache2-dos, arppoison-probe, dict-r2l, neutron-dos, udpstorm-dos |
| \( f_8 \) | udpstorm-dos, selfping-dos |
| \( f_9 \) | apache2-dos, arppoison-probe, crashiis-dos, dict-r2l, dosnuke-dos, fbconfig-u2r, guesstelnet-r2l, imap-r2l, ipsweep-probe, loadmodule-u2r, ls-probe, ncftp-r2l, neutron-dos, pod-dos, portsweep-probe, selfping-dos, smurf-dos, syslogd-dos, udpstorm-dos, warezclient-dos |
| \( f_{10} \) | apache2-dos, smurf-dos, arppoison-probe, pod-dos, dict-r2l |
| \( f_{11} \) | apache2-dos, fbconfig-u2r, loadmodule-u2r, udpstorm-dos |
| \( f_{12} \) | apache2-dos, arppoison-probe, crashiis-dos, dict-r2l, dosnuke-dos, fbconfig-u2r, guesstelnet-r2l, imap-r2l, ipsweep-probe, ls-probe, neutron-dos, pod-dos, portsweep-probe, selfping-dos, smurf-dos, syslogd-dos, udpstorm-dos |
| \( f_{13} \) | apache2-dos, crashiis-dos, dict-r2l, dosnuke-dos, fbconfig-u2r, guesstelnet-r2l, ls-probe, neutron-dos |
| \( f_{14} \) | warezclient-dos, arppoison-probe, pod-dos, ipsweep-probe, udpstorm-dos |
| \( f_{15} \) | apache2-dos, fbconfig-u2r |

Table 6: Number of attack instances detected for each feature and all features correlation for WSD1.

| Features | Total instances | Attacking instances | Normal instances | Total alarms | Detected | False | DR (%) |
|----------|-----------------|---------------------|-----------------|-------------|----------|-------|--------|
| \( f_1 \) | 1320            | 150                 | 1170            | 152         | 40       | 112   | 26.67  |
| \( f_2 \) | 1320            | 150                 | 1170            | 127         | 15       | 112   | 10.0   |
| \( f_3 \) | 1320            | 150                 | 1170            | 140         | 21       | 119   | 14.0   |
| \( f_4 \) | 1320            | 150                 | 1170            | 57          | 3        | 54    | 2.0    |
| \( f_5 \) | 1320            | 150                 | 1170            | 119         | 19       | 100   | 12.67  |
| \( f_6 \) | 1320            | 150                 | 1170            | 216         | 48       | 168   | 32.0   |
| \( f_7 \) | 1320            | 150                 | 1170            | 48          | 13       | 35    | 8.67   |
| \( f_8 \) | 1320            | 150                 | 1170            | 117         | 17       | 100   | 11.33  |
| \( f_9 \) | 1320            | 150                 | 1170            | 750         | 125      | 625   | 83.33  |
| \( f_{10} \) | 1320           | 150                 | 1170            | 25          | 8        | 17    | 5.33   |
| \( f_{11} \) | 1320           | 150                 | 1170            | 60          | 15       | 45    | 10.0   |
| \( f_{12} \) | 1320           | 150                 | 1170            | 479         | 97       | 382   | 64.67  |
| \( f_{13} \) | 1320           | 150                 | 1170            | 188         | 40       | 148   | 26.67  |
| \( f_{14} \) | 1320           | 150                 | 1170            | 90          | 10       | 80    | 10.0   |
| \( f_{15} \) | 1320           | 150                 | 1170            | 23          | 2        | 21    | 1.33   |
| All feature correlation | 1320           | 150                 | 1170            | 894         | 142      | 752   | 94.67  |
Table 7: Number of attack instances detected for each attack type by different basis functions.

| Attack type         | Number of attack instances for each attack type | W5D1 Detected number of attack instances for each attack type |
|---------------------|-----------------------------------------------|-------------------------------------------------------------|
|                     | Daube-chies1 | Coif-lets1 | Sym-lets2 | Discrete Meyer |
| apache2-dos         | 30          | 29         | 29        | 29             | 28             |
| arppoison-probe     | 15          | 15         | 15        | 15             | 15             |
| dict-r2l            | 17          | 17         | 17        | 17             | 17             |
| ncfpt-r2l           | 2           | 2          | 2         | 2              | 0              |
| neptune-dos         | 5           | 5          | 5         | 5              | 5              |
| pod-dos             | 3           | 3          | 0         | 0              | 0              |
| portsweep-probe     | 4           | 2          | 2         | 2              | 1              |
| selfping-dos        | 2           | 2          | 2         | 2              | 2              |
| smurf-dos           | 2           | 2          | 2         | 2              | 1              |
| udpstorm-dos        | 16          | 16         | 15        | 15             | 15             |
| crashis-dos         | 1           | 1          | 1         | 1              | 0              |
| dosnuke-dos         | 2           | 2          | 2         | 1              | 1              |
| fbfconfig-u2r       | 10          | 8          | 7         | 5              | 7              |
| gueststelnet-r2l    | 4           | 4          | 1         | 1              | 1              |
| imap-r2l            | 1           | 1          | 1         | 1              | 0              |
| ipsweep-probe       | 26          | 26         | 25        | 25             | 25             |
| loadmodule-u2r      | 5           | 5          | 0         | 0              | 0              |
| ls-probe            | 2           | 2          | 2         | 2              | 1              |
| syslogd-dos         | 1           | 1          | 1         | 1              | 1              |
| warezclient-dos     | 2           | 2          | 2         | 2              | 1              |

Table 8: Workload of Fred-eZone WiFi network over one day.

| SrcIP  | DstIP  | Flows   | Packets   | Bytes   |
|--------|--------|---------|-----------|---------|
| 1055 K | 1228 K | 30783 K | 994 M     | 500 G   |

collected on a simulated network over a couple of weeks. Evaluating the approaches with the common DARPA dataset is unfair because most of anomaly detection approaches handle the features extracted from the raw packets instead of the original raw TCPDUMP packets. The feature extraction process, however, has an important impact on the final detection result. This is confirmed by comparing two works [46, 47], in which based on the same 1998 DAPRA intrusion detection dataset, the LOF approach (Density-based Local Outliers) is distinctly better than the NN approach (Nearest Neighbor) claimed by Lazarevic et al. in [46], while the LOF, however, is much worse than the NN approach in [47] since two different feature sets are used in these two approaches even those features are both based on the same 1998 DARPA intrusion detection dataset. As a result, the 1999 KDDCUP dataset is set up that is based on 41 common features extracted from the 1998 DARPA intrusion detection dataset. Although the 1999 KDDCUP provides us a common benchmark for evaluating different network anomaly detection approaches under the same conditions, it has been used arbitrarily. For example, some researchers use a part of KDDCUP training dataset for the sake of training and another part for testing, which is not true because there is a separate testing part containing new attacks which do not exist in the training set to see how successful the detection approach is facing with new attacks. Moreover, there are two types of DoS attacks constituting over 71% of the whole KDDCUP testing dataset, which would lead a heavily biased detection result.

During our comparison experiment, we select two typical anomaly detection approaches from both machine learning techniques and signal processing techniques, namely, I-means clustering algorithm [48] and nonparametric CUMulative SUM (CUSUM) algorithm [12]. I-means is a hybrid-clustering algorithm that is built around the k-means algorithm, which can determine systematically the optimal number of clusters for a given dataset. The CUSUM algorithm is an approach to detect a change of the mean value of a stochastic process and it is based on the fact that if a change occurs, the probability distribution of the random sequence will also be changed. Detail information about I-means algorithm and CUSUM can be found in [48] and [12], respectively. To make a fair comparison, we use the same fifteen features as the input for all the three approaches. Table 13 lists the detection results on Day 2, Week 5 (W5D2) in terms of number of attack instances detected for each attack type by different approaches.

There are 24 attack types on W5D2, namely, back, casesen, eject, sformat, smtpwrite, httptunnel, neptune, perl, ppmacro, ps, questel, selfping, syslogd, tcpreset, xterm1, yaga, xsnoop, teardrop, pod, crashis, dosnuke, ipsweep, ncfpt, udpstorm. Total 18 attack types are detected by our wavelet/ARX model except teardrop, ncfpt, udpstorm, casesen, selfping, tcpreset. The CUSUM algorithm detects 11 attack types which are all detected by our approach.
Table 9: Descriptions on attacks identified on the third day in Fred-eZone.

| Attack types          | Number of flows | Volume features          |
|-----------------------|-----------------|--------------------------|
|                       |                 |                          |
| UDP_DoS               | 2               | 313 038                  |
| Multihost_Attack      | 158             | 19 033                   |
| Stealthy_Scan         | 2               | 4 872                    |
| Potential_Scan        | 17              | 724                      |
| Host_Scans            | 44              | 11 226                   |
| Remote_Access_Violation | 4            | 31 441                   |
| **Total**             | **222**         | **1 800 315**            |

Table 10: Number of attack instances detected for each attack type for Fred-Day3.

| Attack Type                  | Fred-Day3         |
|-----------------------------|-------------------|
|                             | Number of attack  |
|                             | instances for each|
|                             | attack type       |
|                             | Detected number   |
|                             | of attack instances|
|                             | for each attack type |
| UDP DoS                     | 1                 |
| Multihost attack            | 1                 |
| Stealthy scan               | 1                 |
| Potential scan              | 1                 |
| Host scans                  | 1                 |
| Remote access violation     | 1                 |

Table 11: Number of attack types detected for each feature for Fred-Day3.

| Feature | Fred-Day3 |
|---------|-----------|
| f_4     | Remote access violation, stealthy scan |
| f_5     | UDP DoS |
| f_6     | Remote access violation |
| f_8     | UDP DoS |
| f_10    | Multihost attack, host scans, stealthy scan |
| f_11 f_13 f_14 | Null |

The I-means detects 14 attack types, in which one attack (i.e., ncftp-r2l) is missed by our approach. Table 14 list the detection rate (DR) for all three approaches in terms of attack type and attack instance.

From Tables 13 and 14, we see that our wavelet model obtains the best detection performance compared to the other two typical machine learning and signal processing techniques.

To conduct a more comprehensive comparison, we also investigate the detection results with the DAPRA intrusion detection dataset by some existing wavelet analysis-based anomaly detection approaches [15, 20, 26]. In [15], Huang et al. evaluate their Waveman framework using three denial-of-service (DoS) attacks from the 1999 DAPRA intrusion detection dataset, namely, neptune, smurf, and mailbomb. They show a large deviation at the locations of the neptune attack start and end, with minimum deviations at all other locations. It is claimed that the entropy-based method and the percentage deviation-based method can be used to detect and analyze network anomalies. The detail anomalies detection results have not been given and are left in their future work. In [20], Dainotti et al. only use part of the normal traffic from the 1999 DARPA dataset to construct normal wavelet signals. Their attacking traces are simulated using existing attack tools, such as TFN2K [49] and Stacheldraht.
Table 12: Number of attack instances detected for each feature and all features correlation for Fred-Day3.

| Features       | Fred-Day3                                      |                |                |                |                |                |                |
|----------------|-----------------------------------------------|----------------|----------------|----------------|----------------|----------------|----------------|
|                | Total instances | Attacking instances | Normal instances | Total alarms | Detected | False | DR (%) |
| $f_4$          | 1440            | 6               | 1434           | 2             | 2           | 0               | 33.3           |
| $f_5$          | 1440            | 6               | 1434           | 1             | 1           | 0               | 16.7           |
| $f_7$          | 1440            | 6               | 1434           | 1             | 1           | 0               | 16.7           |
| $f_8$          | 1440            | 6               | 1434           | 3             | 3           | 0               | 50.0           |
| $f_9$          | 1440            | 6               | 1434           | 0             | 0           | 0               | 0.0            |
| All Feature Correlation | 1440            | 6               | 1434           | 5             | 5           | 0               | 83.3           |

Table 13: Number of attack instances detected for each attack type by different approaches.

| Attack type               | Number of attack instances for each attack type | Detected number of attack instances for each attack type |
|--------------------------|-------------------------------------------------|--------------------------------------------------------|
|                          | W5D2                                            | Wavelet/ARX | CUSUM | I-means |
| xsnoop-r2l                | 2                                               | 2           | 2     | 2       |
| ftpwrite-r2l              | 15                                              | 7           | 5     | 15      |
| back-dos                  | 21                                              | 20          | 11    | 21      |
| neptune-dos               | 18                                              | 15          | 12    | 18      |
| httpunnel-r2l             | 6                                               | 6           | 3     | 5       |
| eject-u2r                 | 17                                              | 17          | 6     | 16      |
| ppmacro-r2l               | 13                                              | 13          | 3     | 9       |
| syslogd-dos               | 1                                               | 1           | 1     | 1       |
| perl-u2r                  | 15                                              | 15          | 3     | 11      |
| Queso-probe               | 1                                               | 1           | 1     | 1       |
| ipsweep-probe             | 20                                              | 9           | 4     | 5       |
| xterm1-u2r                | 41                                              | 23          | 0     | 0       |
| ps-u2r                    | 101                                             | 94          | 0     | 0       |
| pod-dos                   | 1                                               | 1           | 0     | 0       |
| yaga-u2r                  | 43                                              | 29          | 0     | 0       |
| crashiis-dos              | 1                                               | 1           | 0     | 1       |
| fdformat-u2r              | 61                                              | 39          | 0     | 0       |
| dosnuke-dos               | 2                                               | 1           | 0     | 1       |
| ncfp-r2l                  | 2                                               | 0           | 0     | 1       |

Table 14: Detection rate for all three approaches in terms of attack type and instance.

| Approaches   | Performance | DR (%) |
|--------------|-------------|--------|
|              | Attack Type | Attack Instance |
| Wavelet/ARX  | 75.0        | 66.1   |
| CUSUM        | 45.8        | 25.6   |
| I-means      | 58.3        | 54.3   |

[50]. In [26], Rawat and Sastry test their approach on the 10% of the 1999 KDDCUP dataset, which is provided with the full set and consists of almost all the attacks present in the 1998 DARPA dataset with a total of 494,020 records. However, only the detection result for the neptune and smurf attacks are discussed in the paper and only detection results for neptune is showed. Compared to other existing evaluation works, our evaluation is the most completed one since it takes care of the total 55 attack types and 5 full attacking categories. Moreover, during our evaluation, we do not miss any attack instances collected from the 1999 DARPA intrusion detection dataset.

5. Conclusions and Future Work

In this paper, we have proposed a completed network anomaly detection approach based on wavelet transformation and the system identification theory. The input signal is a 15-dimensional feature vector, which is defined to characterize the behavior of the network flows. A prediction model for normal daily traffic is established, in which wavelet coefficients play an important role since we use these normal wavelet coefficients as an external input to an ARX model that predicts the approximation coefficient of the signal yet to be seen. The outputs of this traffic prediction model are
called residuals that measure the difference between normal and anomalous activities. The empirical observations show that the peaks of residuals always stand for the location where attacks occur. As a result, an outlier detection algorithm based on GMM is implemented in order to detect peaks from a set of residuals. Decisions are made based on the results of the proposed outlier detection algorithm. A complete traffic analysis for the 1999 DARPA intrusion detection dataset is conducted using our network anomaly detection approach. To the best of our knowledge, it is the first work to analyze the full 1999 DARPA traffic dataset from the network flow based perspective. The best detection rates in terms of attack types and attack instances are 100% and 94.67%, respectively. That means our approach detects all the attack types appeared on that day and almost 95% attack instances are identified accurately. The experimental comparison with two other typical existing machine learning algorithms (i.e., I-means) and signal processing techniques (nonparametric CUSUM) shows that our approach obtain the best performance.

In the near future, we will focus on applying different wavelet basis functions for modeling the network traffic signals. An interesting problem we attempt to solve is to find whether the different wavelet families have different propensities to different classes of attacks since it implies that these attack classes have core differences in their information which the different wavelet families are bringing to the surface, so that we can unveil a set of questions, for example, "why is a Coiflet better than a Daubechies wavelet for this attack class?", "what is it about this attack class that the Coiflet sees but the Daubechies wavelet does not?", to name a few.

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