Insulator/metal phase transition and colossal magnetoresistance in holographic model

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Within massive gravity, we construct a gravity dual for insulator/metal phase transition and colossal magnetoresistance (CMR) effect found in some manganese oxides materials. In heavy graviton limit, a remarkable magnetic-field-sensitive DC resistivity peak appears at the Curie temperature, where an insulator/metal phase transition happens and the magnetoresistance is scaled with the square of field-induced magnetization. We find that metallic and insulating phases coexist below the Curie point and the relation with the electronic phase separation is discussed.

\section{I. INTRODUCTION}

In recent years, the holographic correspondence [1–4], relating a weak coupling gravitational theory in a (d + 1)-dimensional asymptotically anti-de Sitter (AdS) space-time to a d-dimensional strong coupling conformal field theory (CFT) in the AdS boundary, has been extensively investigated and some remarkable progresses have been made in condensed physics systems [5–9]. For a recent review on the holographic superconductor/superfluid models, please refer to Ref. [10]. Very recently, the present authors and their collaborators have realized the paramagnetism/ferromagnetism and paramagnetism/antiferromagnetism phase transitions in holographic models by introducing a massive 2-form field in an AdS black brane background and some interesting magnetic properties of the models have been investigated in a series of papers [11–17]. In this Letter, we will provide a new application of the holographic AdS/CFT correspondence by implementing the metal/insulator phase transition and the colossal magnetoresistance (CMR) effect found in some manganese oxides materials in a holographic model.

Complex magnetic materials showing strong magnetoresistance have simultaneously been the focus of the attentions of the magnetic recording industry and the study of strongly correlated electron systems. Particularly, the study of the manganites such as $A_1-xB_xMnO_3$ (A = La, Pr, Sm, etc. and B = Ca, Sr, Ba, Pb), which exhibit the “colossal” magnetoresistance effect, is among the main areas of research in strongly correlated electron systems [18–24]. These materials show remarkable magnetoresistivity and an insulator (or semiconductor)/metal phase transition associated with a paramagnetic/ferromagnetic phase transition, which has a completely different physical origin from the “giant” magnetoresistance observed in layered and clustered compounds. These materials are currently being intensively investigated by a sizable fraction of the condensed matter community, and its popularity is reaching the level comparable to the high-temperature superconducting cuprates.

After great efforts in recent years, mainly through computational and mean field studies for realistic models, considerable progress has been achieved in understanding the curious properties of those compounds. However, a fully quantitative understanding of the CMR effect is still a challenge, much work remains to be carried out and it is the subject of current active research [25]. The holographic duality provides an alternative method for this type of strong correlated phenomena. In this paper, we will make a first attempt to build a holographic model to understand the CMR effect.

\section{II. HOLOGRAPHIC MODEL}

Before presenting our holographic model, let us make a brief analysis about how to build a holographic description for such a phenomenon. Firstly, before ferromagnetic phase transition happens, CMR materials are in insulating phase where DC resistivity is finite and increases with decreasing the temperature. So the translation symmetry is broken otherwise no scattering happens and DC resistivity is divergent. More important is that, more and more results from experiments show that the insulating phase in CMR is charge ordered, in which charges are localized and form inhomogeneous structures [21]. To realize the inhomogeneity for the CMR effect is a challenge both in condensed matter theory and holographic description. Fortunately, just as pointed out recently in Ref. [26], momentum relaxation by breaking the translation invariance can be achieved by introducing a mass term of graviton in the bulk so that the macroscopic DC resistance becomes finite. This provides us with a very simple holographic model to study macroscopic DC resistance in some inhomogeneous materials without involving some complicated computations. Secondly, in general, only breaking the translational invariance cannot lead to an insulating resistivity. Meffort and Horowitz [27] proposed a simple framework to have the insulating behavior in general relativity without breaking translational invariance, where a real scalar field is coupled to an U(1) gauge field. But Meffort-Horowitz model is only valid in the case of zero charge density. Thus

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a natural choice to build a holographic insulator model with finite charge density is to consider the Meffort-Horowitz model in a massive gravity theory. Finally, motivated by our previous work about DC resistivity in the paramagnetism/ferromagnetism phase transition in the probe limit \cite{17}, the model with massive 2-form field coupled with Maxwell field shows metallic ferromagnetic phase in low temperatures. This provides us with a mechanism to describe metallic resistivity after the ferromagnetic phase transition.

Based on these considerations, we present the model with the massive 2-form field-Maxwell-dilaton theory in a massive gravity with a negative cosmological constant. The action can be written as,

\begin{equation}
S = \frac{1}{16\pi G} \int d^4x \sqrt{-g} \left[ R + \frac{6}{L^2} - (L_{\text{ins}} + \lambda^2 L_{\text{fer}}) + L_{\text{mg}} \right],
\end{equation}

\begin{align}
L_{\text{ins}} &= e^{-2g_0\psi} F_{\mu\nu} F^{\mu\nu} + \frac{1}{2} \left( \nabla \psi \right)^2 + \frac{m^2_{\psi}}{2} \psi^2, \\
L_{\text{fer}} &= \frac{1}{12} + \frac{m^2_{\psi}}{4} M_{\mu\nu} M^{\mu\nu} + \frac{1}{2} M_{\mu\nu} F_{\mu\nu} + \frac{J^2}{8} V(M), \\
L_{\text{mg}} &= \alpha \nabla^\alpha K + \beta \left[ (\nabla K)^2 - \nabla K^2 \right].
\end{align}

Here \( L \) is the AdS radius and \( G \) is the Newtonian gravitational constant. Without loss of generality, we can set \( L = 1/16\pi G = 1 \). \( \lambda, J, \alpha, \beta \) and \( g_0 \) are all model parameters. \( R \) is scalar curvature, \( A_\mu \) is the U(1) gauge field with field strength \( F_{\mu\nu} = 2\nabla_{[\mu} A_{\nu]} \). \( \psi \) is a dilaton field with squared mass \( m^2_{\psi} \). \( M_{\mu\nu} \) is a 2-form field with squared mass \( m^2_\psi \) and a nonlinear potential \( V(M) \).

The parameter \( \lambda \) can be understood as the coupling strength between the polarization field \( M_{\mu\nu} \) and background Maxwell field strength. In the effective action of string theory, the value of the dilaton coupling parameter is taken to be \( g_0 = 1 \). The case with \( g_0 = \sqrt{3} \) corresponds to the 4-dimensional action by dimensionally reducing from the 5-dimensional Kaluza-Klein theory \cite{32}. Nonetheless, it is helpful to set \( g_0 \) as an arbitrary positive constant here so that we can see what the role of dilaton field plays in the model. In addition, the choice of nonlinear potential \( V(M) \) is not unique. What we need is that there is a critical temperature, below which the xy-component of \( M_{\mu\nu} \) can condense. In this paper, we take the potential as follows,

\begin{equation}
V(M) = (\star M_{\mu\nu} M^{\mu\nu})^2 = [\star (M \wedge M)]^2.
\end{equation}

Here \( \star \) is the Hodge star operator. We choose this form just for simplicity. To be stable for both the bulk and boundary theories when \( \psi = 0 \), we require \( m^2_{\psi} \geq 0 \) for all \( r \) \cite{33, 34}. Following \cite{34}, we take the degenerate reference background with \( f_{xx} = f_{yy} = 1 \) and other components are vanishing. Although the reference background is degenerate, Ref. \cite{34} showed that this two-parameters massive theory is ghost free for the case with \( \beta \) mass term, but it has not yet been proven for the case with \( \alpha \) mass term. Therefore in this paper, we will take \( \alpha = 0 \) in order to avoid possible problems with causality. Note that this reference background leads to that there is a conserved energy but no conserved momentum current in the boundary theory.

### III. BACKGROUND EQUATIONS AND PERTURBATIONS

Now we are in the position to calculate the DC resistivity from our holographic model (1). For this, we assume the dynamic metric has following form,

\begin{equation}
ds^2 = -r^2 f e^{-\chi} dt^2 + \frac{dr^2}{r^2 f} + r^2 (dx^2 + dy^2),
\end{equation}

where \( f \) and \( \chi \) are two functions of \( r \). Suppose the solution has a horizon at \( r_h \), the associated temperature then is \( T = r_h^2 f^2 e^{-\chi/2}/4\pi \). We take the following self-consistent ansatz for matter fields,

\begin{align}
A_\mu &= \phi(r) dt + B x dy, \quad \psi = \psi(r), \\
M_{\mu\nu} &= -\rho(r) dt \wedge dr + \rho(r) dx \wedge dy.
\end{align}

Here \( B \) is a constant magnetic field and it will be viewed as the external magnetic field in the boundary field theory. Put the ansatz and the dynamic metric in (3) into the action (1), we can get a set of ordinary differential
equations. Near the boundary $r \to \infty$, the equations give the following asymptotic solutions for matter fields,

$$
\rho = \rho_+ \left( \frac{r}{r_h} \right)^{1+\delta_1/2} + \rho_- \left( \frac{r}{r_h} \right)^{1-\delta_1/2} + \cdots + \frac{B}{m_\ell^4},
$$

$$
p = \frac{\sigma r_h^2}{m_\ell^4} + \cdots, \quad \phi = \mu - \frac{\sigma r_h}{r} + \cdots,
$$

$$
\psi = \psi_+ \left( \frac{r}{r_h} \right)^{(\delta_2-3)/2} + \psi_- \left( \frac{r}{r_h} \right)^{-(\delta_2+3)/2} + \cdots,
$$

where $\delta_1 = \sqrt{1+4m_\ell^4}$ and $\delta_2 = \sqrt{9+4m_\ell^4}$, $\mu$ is the chemical potential, $\sigma$ is the charge density and $\rho_\pm$ and $\psi_\pm$ are all constants. We impose the regular conditions at the horizon and Dirichlet and source free conditions for matter fields at the boundary of $r \to \infty$, i.e., $\phi = \mu, \psi_+ r_h^{(3-\delta_2)/2} = \Delta$ and $\rho_+ = 0$. Without loss of generality, we can set $\mu = 1$. Note that nontrivial solution for $\psi$ always exists when $g_0 = F_{\mu\nu}$ are both nonzero.

Following Ref. [17], we need that $J < 0$ so that $\rho$ can spontaneously condense below a critical temperature when $B = 0$. We also need that $\delta_1 > 1$ and $\delta_2 < 3$, otherwise the nonlinear terms of $\rho$ and $\psi$ will play more and more important roles when $r \to \infty$, which will break the asymptotic AdS$_4$ geometry of space-time and lead to the instability of the dual theory in the UV region.

Now let us study how DC conductivity is influenced by temperature and external magnetic field in this model. Because of the planar symmetry in the boundary, the conductivity is isotropic. By the AdS/CFT dictionary, we need only turn on a perturbation of gauge field such as $\delta A_x$ along the $x$-direction with ingoing boundary condition at the horizon.

In the case of weak inhomogeneity $m_\ell^4 \ll 1$, the main part of DC resistivity is very simple. In that case, the graviton mass is very small, gravitation fluctuations suffer from smaller scattering than others. So the DC conductivity is dominated by the background geometry. In other words, we can neglect the fluctuations of matter fields when we compute the DC resistivity. Then following Refs. [26, 31], we can find that DC resistivity can be expressed as

$$
R_{\text{right}} = m_g^2/|\mu^2(1-\lambda^2/4m_g^4)| + O(m_g^4). \tag{8}
$$

The more interesting case is the strong inhomogeneous limit, i.e., $m_g^2 \gg 1$, which is the case we are really interested in this paper. In such a limit, graviton has very heavy mass so that it is in fact very hard to be excited by fluctuations. Heavy mass term suppress the fluctuation of gravity so that we can fix the background geometry. In this case, the main part of DC resistivity can be obtained by just considering the fluctuations of matter fields. In the DC limit of $\omega \to 0$, we need only consider three perturbations $\delta A_x = e^{-l_0} \langle \psi \rangle_t$ and $M_{ij} = e_{C_{ij}}(t) r^{-l} + \cdots$ with ingoing conditions at the horizon, where $(i,j) = (r,x), (t,y)$. At the linear order of $e$, we have following equations in the low frequency limit,

$$
C_{\tau y}'' + \frac{1}{2} \chi C_{\tau y}' - \frac{m_\ell^4 C_{\tau y}}{r^2 f} - 4J \psi p C_{\tau y} + O(\omega) = 0, \tag{9a}
$$

$$
m_\ell^4 C_{\tau r} - a_x - 4J e^\chi p C_{\tau y} + O(\omega) = 0, \tag{9b}
$$

$$
[r^2 f e^{-x/2}(e^{-2g_0} \psi a_x' - \lambda^2 C_{\tau r}/4)]' + O(\omega) = 0, \tag{9c}
$$

where a prime stands for the derivative with respect to $r$, and $\psi, p$ and $\rho$ determined by the background equations, $O(\omega)$ is the terms with order of $\omega$, and the other equations of gravity parts and matter parts are order of $O(\omega)$, all of which can be neglected when $\omega \to 0$.

At the boundary $r \to \infty$ with $p, \rho \to 0$, we have the following asymptotic solution for $a_x$,

$$
a_x = a_{x+} + \frac{a_{x-}}{r} + \cdots. \tag{10}
$$

Following the AdS/CFT dictionary, we can obtain that electric current is $\langle J \rangle = a_{x-}$ and the DC resistivity is given by $R = \lim_{\omega \to 0} i a_{x+}/\langle J \rangle$.

In fact, with the “membrane paradigm” of black hole, we can directly obtain the DC conductivity from Eqs. (9) using the method proposed by Iqbal and Liu in Ref. [35]. To see this, we first note that,

$$
\lim_{r \to \infty} r^2 f(a_x' - \lambda^2 C_{\tau r}/4) = -(1 - \lambda^2/4m_g^4)\langle J \rangle. \tag{11}
$$

Eq. (9c) shows that this quantity is conserved along the direction $r$ when $\omega \to 0$. At the horizon, using Eqs. (9) and the fact that $C_{\tau y}$ is regular at the horizon when $\omega \to 0$, we have,

$$
\langle J \rangle = \frac{\lambda^2 m_g^4}{4(m_1^4 + 16J^2 e^{x/2} p_0^2 r_h^2/r_h^4)} \left[ e^{-2g_0} \psi - \frac{\lambda^2 m_g^4}{4(m_1^4 + 16J^2 e^{x/2} p_0^2 r_h^2/r_h^4)} \right]. \tag{12}
$$

Here $\chi_0, \psi_0, p_0$ and $p_0$ are the initial values of $\psi, p$ and $\rho$ at the horizon, respectively. In the low frequency limit, Eq. (9c) implies that the electric field is constant, i.e., $\lim_{r \to r_h} a_x(r) = a_{x+}$. So we obtain the DC resistivity in heavy graviton limit as,

$$
\frac{1}{R_{\text{heavy}}} = (1 - \lambda^2/4m_g^4)^{-1} \left[ e^{-2g_0} \psi - \frac{\lambda^2 m_g^4}{4(m_1^4 + 16J^2 e^{x/2} p_0^2 r_h^2/r_h^4)} \right] + O(1/m_g^4). \tag{13}
$$

As a self-consistent check, we can take $\lambda = 0$. In that case there are only dilaton and Maxwell field. Then we have $R_{\text{heavy}}^{-1} = e^{-2g_0} \psi + O(1/m_g^2)$, which agrees with the exact result $R_{\text{heavy}}^{-1} = Z(\psi_0) + \mu^2/m_g^4$ given in Ref. [31] with dilaton coupling $Z(\psi_0) = e^{-2g_0} \psi_0$. From the expression for DC resistivity, we see that when $R_{\text{heavy}} \sim m_g^2$, the heavy graviton limit is broken. In that case, the fluctuations of metric have to be taken into account.
IV. METAL/INSULATOR PHASE TRANSITION
AND MAGNETORESISTANCE IN STRONG INHOMOGENEITY

The physical phase in different temperature depends on the model parameters. As a typical case, we fix $m_1^2 = 1/3, m_2^2 = -2, m_3^2 = 40, g_0 = 1$ and $\lambda = 3/4$ to compute the DC resistivity at different temperature and small external magnetic field numerically. We first solve the equations of motion from the action and then calculate the DC resistivity numerically. All the results are shown in Fig. 1.

In Fig. 1(a), we plot the DC resistivity at zero magnetic field with different dilaton source $\Delta$. There is a critical $\Delta_c \simeq 0.103$ (we scan $\Delta$ from 5 to -1, numerical precision restricts our ability to check wider region). When $\Delta > \Delta_c$, there is an insulator/metal phase transition. The resistivity shows an insulator's behavior described by dilaton field when $T > T_C$. When the temperature is lowered to the Curie temperature $T_C$, $\rho$ begins to condense spontaneously and a ferromagnetic phase transition happens. Below and near $T_C$, the resistivity decreases when temperature is lowered, which shows a metal's behavior. Though the behavior of DC resistivity is transformed into metallic from insulating, the insulating phase described by dilaton field coexists with ferromagnetic metallic phase in the sample. Numerical results show that two different electronic phases can coexist below the Curie temperature. There is a distinct peak at the temperature where spontaneous magnetization begins to appear and an insulator/metal phase transition happens there. This is just one of characteristic properties of CMR materials in manganese oxides. When $\Delta < \Delta_c$, DC resistivity shows a metallic behavior in the whole temperature (up to the region that numerical computations can be done), though there is still a saltation at $T_C$. What’s more, when a small magnetic field $B$ is turned on, we find that the resistivity is very sensitive to the external magnetic field (see Fig. 1(b)).

Here we emphasize that the heavy graviton limit plays a very important role. Just as mentioned above, for the light graviton case, the behavior of DC resistivity is dominated by fluctuation of graviton, then no such metal/insulator phase transition or CMR effects appear. This is agreement with the fact that the CMR effect is due to the fact that two electronic phases mix with each other and form inhomogeneity in nm scale [19, 21, 36].

It is interesting to compare our holographic results with some experimental data of CMR materials. The resistivity of a typical CMR material $\text{La}_{1-x}\text{Sr}_x\text{MnO}_3$ is shown in Fig. 1(c) and (d). We see that our holographic model gives qualitatively similar results when $x \geq 0.1$, which is a powerful evidence to support that this holographic model is a suitable one to describe the CMR effect. Furthermore, in $\text{La}_{1-x}\text{Sr}_x\text{MnO}_3$, when $x > x_c \simeq 0.2$, the peak of DC resistivity disappears, which is very similar to the case when dilaton source $\Delta < \Delta_c$. So this similarity gives us an explanation for $\Delta_c < \Delta_x < \Delta_m$. We can find from Eq. (13) at the dual boundary field, i.e., dilaton field describes the effects of doping. In addition, we can find from Eq. (13)
the following scaling relation for magnetoresistance (MR) in the case of weak magnetic field and $T \rightarrow T^+$:

$$\text{MR}(B) = 1 - R(B)/R(B=0) \propto \rho_0 \propto B^2. \quad (14)$$

Note that in the region of $T > T_C$, the system is in the paramagnetic phase. Therefore the magnetic moment $N$ is proportional to $B$ in the weak field case. Then Eq. (14) tells us that $\text{MR}(B) \propto N^2$. This result is in complete agreement with the experimental data of CMR materials [18].

V. DISCUSSION

In this paper we have present a gravity dual to the metal/insulator phase transition and found that the model can describe the CMR effect in some manganese oxides materials. The behavior of DC resistivity is in complete agreement with experimental data. The model provides a new example to apply the AdS/CFT correspondence to condensed matter systems. As the first attempt to describe the CMR effect in a holographic setup, more aspects of the model should be further studied. The first one is to study the behavior of DC resistivity in the case with arbitrary graviton mass. For this, we need to consider the perturbations of the gravitational background, which is under investigating. Note that the current model only realizes the macroscopic phenomenon in large scale. It is very interesting to consider whether one can directly realize such local electronic phase separation in a holographic setup with Einstein’s gravity theory rather than massive gravity. For example, we can set the chemical potential periodic in the spatial directions and take the lattice and impurity into account. In those cases, we can expect that $\psi$ and $\rho$ are both inhomogeneous, electronic phase separation may be realized. For this, we have to deal with a set of partially differential equations and the involved numerical computation is extremely non-trivial. We expect it could be reported in future.

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