Limits on the spin-dependent WIMP-nucleon cross-sections from the first science run of the ZEPLIN-III experiment

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We present new experimental constraints on the WIMP-nucleon spin-dependent elastic cross-sections using data from the first science run of ZEPLIN-III, a two-phase xenon experiment searching for galactic dark matter WIMPs based at the Boulby mine. Analysis of ~450 kg-days fiducial exposure revealed a most likely signal of zero events, leading to a 90%-confidence upper limit on the pure WIMP-neutron cross-section of $\sigma_n = 1.8 \times 10^{-2}$ pb at 55 GeV/c² WIMP mass. Recent calculations of the nuclear spin structure based on the Bonn CD nucleon-nucleon potential were used for the odd-neutron isotopes $^{129}$Xe and $^{131}$Xe. These indicate that the sensitivity of xenon targets to the spin-dependent WIMP-proton interaction is much lower than implied by previous calculations, whereas the WIMP-neutron sensitivity is impaired only by a factor of ~2.

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ZEPLIN-III has recently completed its first run at the Boulby Underground Laboratory (UK) searching for weakly interacting massive particles (WIMPs), which have been proposed to explain the non-baryonic cold dark matter in the Universe. In several supersymmetry (SUSY) extensions to the Standard Model of particle physics, the lightest supersymmetric particle (LSP) is stable and its relic abundance could account for the matter content observed today. In most SUSY scenarios this particle is the neutralino, $\tilde{\chi}$, which is a linear combination of the SUSY partners of the electroweak gauge bosons (gauginos) and Higgs bosons (higgsinos). Neutralinos are expected to scatter elastically from ordinary matter, producing low-energy nuclear recoils, predominantly through scalar (or spin-independent, SI) interactions. This is especially so for heavier elements (A > 30, with A the number of nucleons), for which the scattering involves the entire nucleus rather than individual nucleons. This coherence enhancement of the scalar term in the interaction cross-section is proportional to $A^2$. Our SI result excludes a WIMP-nucleon cross-section above $7.7 \times 10^{-8}$ pb for 55 GeV/c² mass with 90% confidence.

Nonetheless, axial-vector (or spin-dependent, SD) interactions could dominate in some SUSY scenarios in regions where the SI term is suppressed. In addition, interpretation of the DAMA annual modulation in terms of nuclear recoils caused by a dominant SD interaction has remained viable for WIMP masses below ~15 GeV until recently. It is therefore important to continue pursuing the search in the SD channel. Xenon targets have good sensitivity to the WIMP-neutron interaction since approximately half of natural abundance consists of the odd-neutron isotopes $^{129}$Xe and $^{131}$Xe (the proton interaction is highly suppressed for these isotopes, and neither is likely in the even-even nuclei).

It is also possible that a SD inelastic interaction with these nuclei could be significant for relatively heavy WIMPs. Deexcitation of low-lying nuclear states in $^{129}$Xe and $^{131}$Xe (emitting 39.6 keV and 80.2 keV $\gamma$-rays, respectively) provides a detection mechanism with low effective energy threshold, since the $\gamma$-rays can be efficiently detected. Although neutrons also scatter inelastically producing the same signatures, differences in spatial distribution between signal and background might be exploited in very large detectors – assuming that the dominant $\gamma$-ray backgrounds could be suitably mitigated.

Most direct search experiments are still focused on detecting nuclear recoils down to ~keV energies; this is so in the case described in this Letter.

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WIMP search experiments propose to measure the total WIMP-nucleus elastic cross-section, $\sigma_A$. Assuming dominance of either the SI or the SD term, one can write:

$$\sigma_A = 4G_F^2\mu_A^2 C_A,$$

where $G_F$ is the Fermi weak-coupling constant, $\mu_A$ is the reduced mass of the WIMP-nucleus system, and $C_A$ is an enhancement factor which depends on the type of interaction and, possibly, the WIMP composition. For the SI case, $C_A \propto A^2$ (i.e. $C_A$ is model-independent for Majorana WIMPs). For a dominant SD case, $C_A$ involves the total nuclear spin $J$ instead:

$$C_A = \frac{8}{\pi} (a_p\langle S_p \rangle + a_n\langle S_n \rangle)^2 \frac{J+1}{J},$$

where $\langle S_{p,n} \rangle$ are the expectation values for the proton or neutron spins averaged over the nucleus and $a_{p,n}$ are the effective WIMP-nucleon coupling constants. The latter depend on the WIMP particle content (e.g. more higgsino- or gaugino-like) as well as the quark spin distributions inside the nucleons.

Two spin distribution calculations were adopted, both based on the nuclear shell model but using different nucleon-nucleon ($nn$) potentials (see, e.g., reviews [10, 11]). Their ability to reproduce experimental measurements of the magnetic moment is the standard benchmark, as this observable is reasonably similar to the WIMP-nucleus scattering matrix element. For comparison with other Xe experiments we use spin structures with the Bonn A potential for both isotopes [12]. Agreement of the magnetic moment (using effective $g$-factors) is quite reasonable: within 19% and 8% for $^{129}$Xe and $^{131}$Xe, respectively. In addition, new calculations based on the Bonn-CD G-matrix have become available which improve on these figures significantly (to 1% and 2%) for both isotopes [8]. The spin expectation values $\langle S_{p,n} \rangle$ are given in Table I for both cases.

In order to compare with an experimental result a nuclear form factor, $F^2(q)$, must be assumed at momentum transfer $q > 0$ to account for finite nuclear size. Although cross-sections are conventionally given in the limit of zero momentum transfer (the ‘standard cross-section’), $F^2(q)$ must be factored into (1) to describe the interaction with a particular nucleus. The definition of $C_A$ in (2) justifies the use of a normalised form factor $F^2(q)$=$S(q)/S(0)$, where $S(q)$ folds the spin structure functions $S_{j\mu}(q)$ with an arbitrary neutralino composition in the isospin convention. The related functions $F_{\mu\nu}(u)$ derived with Bonn CD [6] were converted into the same $S_{j\mu}(q)$ normalisation used with Bonn A [12] by employing Eq. (18) in Ref. [13] and then parametrised with a 6th-order polynomial for low $q$. As noted in Ref. [9], the new calculation gives smaller spin structures than those found for simpler models: by a factor of ~2 for Xe$^{129}$ and ~4 for Xe$^{131}$ at low $q$. More significantly, the spin factors are also smaller, in particular $\langle S_p \rangle$.

### TABLE I: Xe isotope parameters: nuclear spin $J$, isotopic fraction (nat. abundance), effective exposure and spin factors $\langle S_{p,n} \rangle$ with Bonn A [12] and Bonn CD [6] $nn$ potentials.

| Isotope | $J$ | Isotopic Fraction (%) | $\langle S_p \rangle$ | $\langle S_n \rangle$ | $\langle S_{p,n} \rangle$ |
|---------|-----|----------------------|---------------------|---------------------|---------------------|
| $^{129}$Xe | 2 | 1/2 29.5 (26.4) | 37.7 | 0.359 | 0.028 | 0.273 | -0.0019 |
| $^{131}$Xe | 3/2 | 23.7 (21.2) | 33.7 | -0.227 | -0.009 | -0.125 | -0.00069 |

Calculating the cross-section per nucleon allows comparison of different target materials and with theoretical model predictions, which are usually computed for free protons and neutrons. This conversion is not straightforward for the SD case since the cross-section has contributions from both proton and neutron terms, as indicated explicitly in (2). In addition, $F^2(q)$ is similarly contaminated by both couplings. A simple approach exists that allows a straightforward calculation in a model-independent way by assuming that WIMPs couple predominantly to protons or neutrons [14]. By setting, in turn, $a_n=0$ and $a_p=0$, no assumption is required as to the neutralino composition, either explicitly in the standard cross-section or in the form factor. In this instance one may write, in the limit of zero momentum transfer:

$$\frac{\sigma_{p,n}}{\sigma_A} = \frac{3 \mu_{p,n}^2}{4 \mu_A^2} \frac{1}{\langle S_{p,n} \rangle^2} \frac{J}{J+1},$$

where $\mu_{p,n}$ is the WIMP-nucleon reduced mass. Once $\sigma_A$ is obtained from experimental limits on the allowed nuclear recoil spectrum, (3) is used to calculate the corresponding SD cross-section for each isotope, $\sigma_{p,n}^{129}$ and $\sigma_{p,n}^{131}$. These are combined to obtain the total cross-sections:

$$\langle \sigma_{p,n} \rangle^{-1} = (\sigma_{p,n}^{129})^{-1} + (\sigma_{p,n}^{131})^{-1}.$$

ZEPLIN-III is a two-phase xenon time projection chamber operating 1100 m underground at the Boulby mine. It is able to discriminate between nuclear recoil signals and the more prevalent electron recoil background by measuring both the scintillation light (S1) and the ionisation charge (S2) produced by interactions in its 12 kg liquid xenon target. 3D reconstruction of the interaction vertex, a strong electric field in the liquid (3.9 kV/cm) and a geometry which avoids surfaces near a central fiducial region allow powerful discrimination down to low energies. Data analysis procedures are detailed with our SI result [2] and briefly summarised here. The instrument is further described in Refs. [15, 16].

A WIMP acceptance region was defined in the range [10.7,30.2] keV recoil energy and [$\mu$–2$\sigma$,\$\mu$] in the $\log_{10}$ (S2/S1) discrimination parameter, where $\mu$ and $\sigma$ describe the means and standard deviations of log-normal distributions fitted to the nuclear recoil population produced by elastic neutron scattering over that energy range. An effective exposure of 128.7 kg-days was accumulated during the 83-day science run between 27th Feb...
and 20th May 2008. This exposure is derived from a fiducial mass of 6.5 kg, defining a total ‘geometrical’ exposure of 454 kg-days, and a factor subsuming all energy-independent hardware and software inefficiencies (and the restricted acceptance). An energy-dependent detection efficiency, which reaches unity near 14 keV recoil energy, is applied separately. Conversion between visible and nuclear recoil energies utilises the varying quenching factor (QF) discussed in Ref. [2]. The exposure of the odd-neutron isotopes reflects their relative abundance. Our xenon was depleted from high-mass isotopes, especially 136Xe used in 0νββ-decay experiments. This enhances slightly the isotopic composition in 129Xe and 131Xe relative to natural abundance (see Table I), as confirmed by residual gas analysis using mass-spectroscopy.

Seven events were observed in the acceptance region, all near the upper boundary of the discrimination parameter. These were shown to be statistically consistent with the tail of the electron-recoil background population. To test this hypothesis in the presence of a hypothetical WIMP signal, a maximum likelihood analysis was performed on the acceptance region. This returned a most likely signal of zero WIMP events, with 90% upper limits increasing from 2.45 to 3.0 events with increasing WIMP mass. The experimental limit on the WIMP-nucleus cross-section, $\sigma_A$, was calculated as described Ref. [17]. We assumed an isothermal dark matter halo with truncated Maxwellian velocity distribution with characteristic velocity $v_0=220$ km/s, galaxy escape velocity $v_{esc}=600$ km/s, Earth velocity $v_E=230$ km/s and WIMP mass density $\rho_0=0.3$ GeV/cm$^3$. The limit on the differential recoil spectrum was corrected by the normalised nuclear form factor and detector parameters such as energy resolution and detection efficiency.

The SD cross-section limits, with no assumption on the coupling strength to neutrons and protons, are shown in Figure 1 for the two spin structures. Values at 55 GeV/c$^2$ WIMP mass, the minimum of the curves, are given in Table II. Our Bonn A result surpasses that from XENON10 [18] above 100 GeV (taking into account new QF measurements for xenon [19]). Together these experiments place the world’s most stringent limit on $\sigma_n$, when this $nn$ potential is assumed. However, Bonn CD affects these limits unfavourably: $\sigma_n$ is just under twice higher, but $\sigma_p$ increases by orders of magnitude, virtually eliminating the sensitivity to WIMP-proton scattering (this curve is not shown in the figure as it would fit poorly within the range plotted). Naturally, these corrections apply to all xenon detectors. We note that comparison with other experiments is not always straightforward: i) different spin structures may be used for the same isotopes, as new calculations are still emerging; ii) the model-independent approach of Ref. [14] is not used universally (e.g. a combined SI and SD limit is extracted in HDMS, where a novel background subtraction technique is also employed [20]); and iii) statistical significance may vary, as with the XENON10 result, for which a CL$<90\%$ is acknowledged for the upper limit (c.f. note [26] in [21]).

The allowed region of $\sigma_n - \sigma_p$ parameter space can be derived from the experimental cross-section limits [14]:

$$\sum_i \left( \frac{\sigma_p}{\sqrt{\sigma_p}} \pm \frac{\sigma_n}{\sqrt{\sigma_n}} \right)^2 \leq \frac{\pi}{24G_F^2 \mu_p^2}$$

(4)

where $i$ labels the two Xe isotopes, and the sign in parenthesis is that of $\langle S_p \rangle/\langle S_n \rangle$. For xenon and other multi-isotope targets, (4) defines an ellipse – albeit an elongated one – which reduces to two parallel lines for single-isotope experiments. The region allowed by each ex-
TABLE II: Spin-dependent cross-section limits (pb) at $M_W = 55$ GeV for $^{129}$Xe and $^{131}$Xe, and the combined ZEPLIN-III result.

|          | $\sigma^{129}_p$ | $\sigma^{129}_n$ | $\sigma^{131}_p$ | $\sigma^{131}_n$ | $\sigma_p$ | $\sigma_n$ |
|----------|------------------|------------------|------------------|------------------|------------|------------|
| Bonn A   | $1.2 \times 10^{-2}$ | $8.3 \times 10^{-1}$ | $5.7 \times 10^{-2}$ | $5.8 \times 10^{-1}$ | $9.7 \times 10^{-3}$ | $7.2 \times 10^{-4}$ |
| Bonn CD  | $2.0 \times 10^{-2}$ | $4.8 \times 10^{-2}$ | $1.5 \times 10^{-1}$ | $2.0 \times 10^{-3}$ | $1.8 \times 10^{-2}$ | $3.9 \times 10^{-2}$ |

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FIG. 2: Allowed regions in the $a_n - a_p$ parameter space for 50 GeV WIMP mass.

Experiment lies within the corresponding ellipse. Figure 2 shows our Bonn CD result (nearly vertical lines, reflecting the poor constraint on $a_p$) for a reference WIMP mass of 50 GeV/c$^2$ (the cross-sections coincide with those in Table II within the precision shown). The Bonn A result (not shown) is very similar to that from XENON10.

In conclusion, new experimental limits on the SD WIMP-nucleon cross-section are placed by the first science run of ZEPLIN-III operating at Boulby. A fiducial exposure of ~450 kg-days revealed a most likely signal of zero events, which allow 90% CL exclusion of the pure WIMP-neutron cross-section above $\sigma_n = 1.8 \times 10^{-2}$ pb for 55 GeV/c$^2$ WIMP mass. New spin structure calculations based on the Bonn CD $nn$ potential were used for $^{129}$Xe and $^{131}$Xe. These increase the cross-section limits relative to previous calculations – quite dramatically in the case of the proton. Xenon targets are still the very sensitive to the WIMP-neutron interaction. Our result adds weight to the exclusion of the DAMA evidence region for a 50 GeV/c$^2$ WIMP causing nuclear recoils. Theoretical predictions in the CMSSM [32] point to $\tilde{\chi}$-nucleon cross-sections below $3 \times 10^{-3}$ pb near 100 GeV mass at 95% CL. ZEPLIN-III, XENON10 and CDMS-II provide the leading constraint on SD $\tilde{\chi}$-neutron scattering at that mass, nearly missing that probability boundary. Experimental efforts are still far from probing the favoured parameter space for the $\tilde{\chi}$-proton interaction (the CMSSM best-fit regions suggest $\sim 1 \times 10^{-4}$ pb for both nucleons).