The First Stars: formation under cosmic ray feedback

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ABSTRACT
We explore the impact of a cosmic ray (CR) background generated by supernova explosions from the first stars on star-forming metal-free gas in a minihalo at $z \sim 25$. Starting from cosmological initial conditions, we use the smoothed particle hydrodynamics code GADGET-2 to follow gas collapsing under the influence of a CR background up to densities of $n = 10^{12}$ cm$^{-3}$, at which point we form sink particles. Using a suite of simulations with two sets of initial conditions and employing a range of CR background models, we follow each simulation for 5000 yr after the first sink forms. CRs both heat and ionise the gas, boosting H$_2$ formation. Additional H$_2$ enhances the cooling efficiency of the gas, allowing it to fulfil the Rees-Ostriker criterion sooner and expediting the collapse, such that each simulation reaches high densities at a different epoch. As it exits the loitering phase, the thermodynamic path of the collapsing gas converges to that seen in the absence of any CR background. By the time the gas approaches sink formation densities, the thermodynamic state of the gas is thus remarkably similar across all simulations. This leads to a robust characteristic mass that is largely independent of the CR background, of order $\sim$ a few $\times 10^3$ M$_\odot$ even as the CR background strength varies by five orders of magnitude.

Key words: stars: formation — stars: Population III — cosmology: theory — early Universe — dark ages, first stars

1 INTRODUCTION
Cosmic rays (CRs) have long been known to play an important role in the complex physics and chemistry of the interstellar medium (ISM) in local galaxies (Spitzer & Tomasko 1968; Spitzer & Scott 1969; Glassgold & Langer 1973; Goldsmith & Langer 1978; Cravens & Dalgarno 1978; Mannheim & Schlickeiser 1994; Tielens 2005 recently reviewed by Strong et al. 2007; Grenier et al. 2015). They are an effective source of ionisation and heating in various environments, from preheating the primordial intergalactic medium (IGM; Sazonov & Sunyaev 2015), to driving outflows in the diffuse ISM (e.g., Enßlin et al. 2007; Unbelgas et al. 2008; Salem & Bryan 2014; Hamasz et al. 2013; Booth et al. 2013; Salem et al. 2014), to providing an important (often dominant) source of heating and ionisation in deeply embedded gas clouds and protostellar discs (Spitzer 1978; Dalgarno et al. 1999; Indriolo et al. 2009; Padovani et al. 2009; Glassgold et al. 2012; Padovani et al. 2013; 2015).

CRs are particularly interesting in the context of Population III (Pop III) star formation, as they provide a continually replenished source of free electrons, enhancing the formation of molecular hydrogen—the only coolant available in primordial gas (Abel et al. 1997; Galli & Palla 1998; Bromm et al. 2002). This enhances the ability of the gas to cool, modifying the characteristic density and temperature at which runaway gravitational collapse sets in, and possibly the characteristic mass of the stars thus formed. The characteristic mass of Pop III is critical, as it largely controls the extent to which the first stars influence their environment, determining both their total luminosity and ionising radiation output (Schaerer 2002), in addition to the details of their eventual demise (Heger et al. 2003; Heger & Woosley 2010; Maeder & Meynet 2012). As such, a thorough understanding of how the very first stars impact subsequent episodes of metal-free star formation—sometimes referred to as Pop III.1 and Pop III.2, respectively (McKee & Tan 2008)—is crucial to developing a comprehensive picture of cosmic evolution.

In the absence of any feedback, pioneering numerical studies suggested that the very first stars were quite massive—on the order of 100 M$_\odot$ (e.g., Bromm et al. 1999; 2002; Abel et al. 2002; Yoshida et al. 2003; Bromm & Larson 2004; Yoshida et al. 2006; O’Shea & Norman 2007). However, more recent simulations, aided by increased resolution, have found that significant fragmentation occurs during the star formation process (Stacy et al. 2010; Clark et al. 2011; Greif et al. 2011; Stacy & Bromm 2013; Hirano et al. 2014; Hosokawa et al. 2015), leading to the emerging consensus that the Pop III initial mass func-
tion (IMF) was somewhat top-heavy with a characteristic mass of $\sim \times 10^4 M_\odot$ [Bromm 2013]. While the contribution these stars make to chemical enrichment [Madau et al. 2001; Mori et al. 2002; Bromm et al. 2003; Beger et al. 2003; Umesa & Nomoto 2003; Tornatore et al. 2007; Greif et al. 2007; Greif et al. 2010; Wisse & Abel 2008; Mao et al. 2011] recently reviewed in Karlsson et al. 2013 and reionisation (Kitayama et al. 2004; Sokasian et al. 2004; Whalen et al. 2004; Alvarez et al. 2006; Johnson et al. 2007; Robertson et al. 2010) have been well studied, the consequences for Pop III stars forming in neighbouring minihaloes have been less thoroughly explored.

As Pop III stars form in a predominantly neutral medium, the majority of their ionising output is absorbed, allowing only radiation less energetic than the Lyman-α transition to escape the immediate vicinity of the star-forming halo. While far-ultraviolet radiation in the Lyman-Werner (LW) bands (11.2 – 13.6 eV) lacks sufficient energy to interact with atomic hydrogen, it can still effectively dissociate molecular hydrogen. However, studies have found that the expected mean value of such radiation is far below the critical LW flux required to suppress H$_2$ cooling (Dijkstra et al. 2005). At the high energy end, the neutral hydrogen cross section for X-rays and cosmic rays is small, allowing them to easily escape their host minihaloes. We recently investigated the impact of a cosmic X-ray background generated by high-mass X-ray binaries on primordial star formation [Hummel et al. 2015], here we focus on the impact of a CR background consisting of particles accelerated in supernova shock waves via the first-order Fermi process (see Section 2).

While the uncertainties involved in estimating the strength of the high-z CR background are huge, measurements of the $^6$Li abundance from metal-poor stars in the Galactic halo provide a useful constraint: the observed abundance of $^6$Li is approximately 1000 times higher than predicted by big bang nucleosynthesis [Asplund et al. 2006], strong evidence for the existence of a CR spallation channel to provide a $^6$Li bedrock abundance prior to the bulk of star formation [Rollinde et al. 2005; 2006]. Production of this first pervasive CR background by shock-acceleration in Pop III supernovae dovetails nicely with the upper limits this places on the CR energy density at high redshifts [Rollinde et al. 2006].

Early studies of the impact of CRs on primordial star formation focused on the production of ultra-high-energy CRs (UHECRs) by the decay of ultra-heavy X particles (Shchekinov & Vasiliev 2004; Vasiliev & Shchekinov 2006; Ripamonti et al. 2007). With energies above the Greisen-Zatsepin-Kuzmin (GZK) cutoff [Greisen 1966; Zatsepin & Kuzmin 1966], UHECRs interact with the cosmic microwave background (CMB) to produce ionising photons, which in turn enhance the free electron fraction of the gas. Other work investigated the direct collisional ionisation of neutral hydrogen by SN shock-generated CRs, using one-zone models to determine the impact of a CR background on the chemical and thermal evolution of the gas in a minihalo [Stacy & Bromm 2007; Jasche et al. 2007]. These studies found that the presence of a CR background enhanced molecular hydrogen formation in the minihalo, cooling the gas and lowering the Jeans mass, and by extension, the characteristic mass of the stars formed. We expand upon these one-zone models, using three-dimensional ab initio cosmological simulations to investigate the impact of a CR background on Pop III stars forming in a minihalo.

This paper is organized as follows: In Section 2, we provide the cosmological context for this study, estimating the expected intensity of the CR background. Our numerical methodology is described in Section 3, while our results are presented in Section 4. Finally, our conclusions are gathered in Section 5. Throughout this paper we adopt a $\Lambda$CDM model of hierarchical structure formation, using the following cosmological parameters, consistent with the latest measurements from the Planck Collaboration [Ade et al. 2015]: $\Omega_{\Lambda} = 0.7$, $\Omega_m = 0.3$, $\Omega_b = 0.04$, and $H_0 = 70 \text{km s}^{-1}\text{Mpc}^{-1}$.

## 2 COSMIC RAYS IN THE EARLY UNIVERSE

While there are several possible sources of CRs at high redshifts including primordial black holes, topological defects, supermassive particles, and structure formation shocks, the most likely source in the early Universe is supernova (SN) explosions (e.g., Ginzburg & Syrovatskii 1969; Biermann & Sigl 2001; Stanev 2004; Pfrommer et al. 2006), wherein CRs are accelerated by the SN shock wave via the first-order Fermi process (e.g., ?). In this scenario, high-energy particles diffuse back and forth across the shock front, increasing their energy by a small percentage each time, and resulting in a differential spectrum of CR number density per energy (Longair 1994) of the form

\[
\frac{dn_{\text{CR}}}{d\epsilon} = \frac{n_{\text{norm}}}{\epsilon_{\text{min}}} \left(\frac{\epsilon}{\epsilon_{\text{min}}}\right)^{-2},
\]

where $n_{\text{CR}}$ is the CR number density, $\epsilon$ is the kinetic energy of the CR, $\epsilon_{\text{min}}$ is the low-energy cutoff of the CR spectrum, and $n_{\text{norm}}$ is a normalising density factor.

The value of $\epsilon_{\text{min}}$ is crucial, as the ionisation cross-section of non-relativistic CRs varies roughly as $\epsilon^{-1}$ for $\epsilon \gtrsim 10^6$ eV. Higher energy CRs thus travel much farther between interactions and are less able to effectively deposit their energy into the gas, such that the low-energy end of the CR spectrum provides the majority of the ionisation and heating. While estimates of the lowest possible energy CR protons could gain in a SN shock wave vary significantly, below $10^6$ eV the velocity of the CR drops below the approximate orbital velocity of electrons in the ground state of atomic hydrogen, and the interaction cross-section diminishes rapidly (Schlickeiser 2002).

We therefore employ $\epsilon_{\text{min}} = 10^6$ eV as the lower bound for the CR background in our simulations. While CRs with energies below $10^6$ eV may account for $\sim 5$–$50$ percent of the CR energy budget, they also deposit a substantial fraction of their energy into the IGM [Sazonov & Sunyaev 2015]. Consequently, they are unable to efficiently contribute to the build-up of a large-scale CR background. We thus neglect the contribution such CRs make to the ionisation and heating of primordial gas. However, this introduces only minor errors, as shown by Stacy & Bromm 2007. Using one-zone models, they found that extending the CR spectrum to as low as $\epsilon_{\text{min}} = 10^3$ eV altered the resulting ionisation and heating rates by less than a factor of two. It should also be noted that the uncertainty in $\epsilon_{\text{min}}$ is on par with that...
for the fraction of the SN energy going into CR production, $f_{\text{CR}}$, which is expected to be $\sim 10^{-20}$ percent (Caprioli & Spitkovsky 2014). Here we assume $f_{\text{CR}} = 0.1$.

The upper limit of the CR energy spectrum $\epsilon_{\text{max}}$ depends on the strength of the ambient magnetic field in the local ISM, as the Fermi acceleration process is linearly dependent on the magnetic field through which the SN shock wave propagates. As the strength, generation mechanism, and distribution of magnetic fields in the early Universe remain highly uncertain (Durrer & Neronov 2013), we set $\epsilon_{\text{max}} = 10^{16}$ eV, a typical maximum value from Fermi acceleration theory in SN shocks (e.g., Blandford & Eschier 1987). So long as $\epsilon_{\text{max}}$ is below the GZK cutoff, $\epsilon_{\text{GZK}}$, at that redshift, given by $\epsilon_{\text{GZK}} = 5 \times 10^{19}$ eV $(1 + z)$, the precise value of $\epsilon_{\text{max}}$ is not crucial, since the great majority of the heating and ionisation is provided by CRs near $\epsilon_{\text{min}}$.

Magnetic fields also play an important role in isotropising the CR background. We may estimate the effective mean free path over which a CR can freely propagate before being significantly impacted by the presence of a magnetic field B using the Larmor radius $r_L$, where for a proton,

$$r_L = \frac{\gamma m_p c^2}{e B}.$$  

(3)

Here, $\gamma$ is the Lorentz factor of the CR; $m_p$, the proton mass; $e$, the proton charge; $c$, the speed of light, and $\beta c$ the CR velocity. The CR background at redshift $z$ for protons with energy $\epsilon$ may then be considered fully isotropic if $r_L(\epsilon) \ll D_H(z)$ where $D_H(z)$ is the Hubble distance at that epoch. Recent observations have placed lower bounds on the modern-day intergalactic magnetic field strength ranging from $10^{-18}$ G (Dermer et al. 2011) to $3 \times 10^{-16}$ G (Neronov & Voïk 2010), while other estimates place the field strength as high as $10^{-15}$ G (Ando & Kusenko 2010). Simply accounting for flux freezing, the magnetic field at redshift $z$ is given by

$$B(z) = B_0 (1 + z)^2,$$  

(4)

where $B_0$ is the magnetic field at the current epoch. The magnetic field strength in the IGM at $z = 20$ then was likely in the range $4 \times 10^{-16}$ to $4 \times 10^{-13}$ G. The magnetic field strength required to fully randomize the path of a $10^{15}$ eV CR proton is $\sim 10^{-14}$ G; we may therefore assume the CR background is fully isotropic to the limit of our CR spectrum. The Larmor radius for a $10^6$ eV CR proton in a $10^{-15}$ G magnetic field, on the other hand, is $\sim 10$ pc. While unable to freely propagate, under the assumption that magnetic fields at these redshifts are unordered on pc scales, such CRs will diffuse through the IGM with a diffusion coefficient $D = c r_L$. Given that the typical physical distance $L$ between minihaloes at $z = 20$—derived from the Press-Schechter (1974) formalism—is $\sim 5$ kpc, the diffusion time between minihaloes, $t_{\text{diff}} = L^2 / D$, is of order $10^{14}$ s, less than the Hubble time at this epoch. $10^6$ eV CRs are thus able to build up a locally isotropic background on scales larger than the typical distance between minihaloes. On the scale of our simulation boxes (see Section 3.1), CRs are thus able to build up an effectively uniform and isotropic background from $10^6$ to $10^{15}$ eV, an assumption we make throughout the remainder of our analysis.

Normalising the differential CR spectrum with the aforementioned limits $\epsilon_{\text{min}}$ and $\epsilon_{\text{max}}$ to the total energy density in cosmic rays, $u_{\text{CR}}$, results in a CR energy spectrum increasing over cosmic time in the following fashion:

$$\frac{\text{d}n_{\text{CR}}}{\text{d}\epsilon} (z) = \frac{u_{\text{CR}} (z)}{\epsilon_{\text{min}} \ln \epsilon_{\text{max}} / \epsilon_{\text{min}}} \left( \frac{\epsilon}{\epsilon_{\text{min}}} \right)^{-2}.$$  

(5)

Here we estimate $u_{\text{CR}}$ as follows:

$$u_{\text{CR}} (z) = f_{\text{CR}} E_{\text{SN}} f_{\text{SN}} \Psi_\star (z) t_H (z) (1 + z)^3,$$  

(6)

where $f_{\text{CR}}$ is the fraction of the SN explosion energy $E_{\text{SN}}$ going into CR production, $f_{\text{SN}}$ is the mass fraction of stars formed which die as SNe, and $\Psi_\star (z)$ is the comoving star formation rate density (SFRD) as a function of redshift, which we assume to be constant over a Hubble time $t_H$. The factor of $(1 + z)^3$ accounts for the conversion from a comoving SFRD to a physical energy density. As in Hummel et al. (2015), we base our estimate of $u_{\text{CR}} (z)$ on the Pop III SFRD calculated by Greif & Bromm (2006), but see Campisi et al. (2011) for a more recent calculation.

The mass fraction of Pop III stars dying as SNe depends strongly on their IMF, and while the complex physical processes at play in gas collapsing from IGM to protostellar densities have so far prevented a definitive answer to this question, the emerging consensus is that the Pop III IMF was somewhat top-heavy with a characteristic mass of $\sim 10^5 M_\odot$ (Bromm 2013). Given this, we assume one SN is produced for every $50 M_\odot$ of stars formed and each SN-producing star dies quickly as a core-collapse explosion with $E_{\text{SN}} = 10^{51}$ erg, 10 percent of which goes into CR production.

This fiducial estimate for $u_{\text{CR}} (z)$—henceforth referred to as model $u_0$—is shown in Figure 1 where we compare the energy density in CRs to the gas thermal energy density in the IGM, the range of estimates for the IGM magnetic field energy density, and the energy density of the cosmic microwave background. We also mark the most conservative upper limits placed on $u_{\text{CR}}$ by Rolinde et al. (2006), calculated using the observed overabundance of $^6$Li compared to big bang nucleosynthesis. Given the huge uncertainties inherent in estimating the strength of the high-$z$ CR background, we also consider five additional models with $10^3$, $10^7$, $10^9$, and $10^{15}$ times the energy density of model $u_0$, as shown in Figure 1. This allows us to bracket the plausible range of energy densities, from values comparable to the IGM thermal energy density to just below the upper limits from $^6$Li abundance measurements.

### 3 NUMERICAL METHODOLOGY

Using the well-tested $N$-body smoothed particle hydrodynamics (SPH) code GADGET-2 (Springel 2005), we perform our simulations using the same chemistry network and sink particle method as described in Hummel et al. (2015); the relevant details are summarized below. In addition to using the same initial conditions as in Hummel et al. (2015) to allow for a comparison of the impact of X-rays versus cosmic rays on the primordial gas, we perform a second suite of simulations using new initial conditions. The minihalo in
3.1 Initial Setup

The first set of simulations (henceforth referred to as Halo 1) use the same initial conditions as Hummel et al. (2015) and Stacy et al. (2010), and are initialised at \( z = 100 \) in a 140 comoving kpc box with periodic boundary conditions. To accelerate structure formation within the simulation box an artificially enhanced normalisation of the power spectrum, \( \sigma_8 = 1.4 \), was used, but the simulations are otherwise initialised in accordance with a ΛCDM model of hierarchical structure formation. For a discussion of the validity of this choice, see Stacy et al. (2010). High resolution in these simulations is achieved using a standard hierarchical zoom-in technique, with nested levels of refinement at 40, 30, and 20 kpc (comoving). Using this technique, the highest resolution SPH particles have a mass \( m_{\text{SPH}} = 0.015 M_\odot \), yielding a minimum mass resolution \( M_{\text{res}} \approx 1.5N_{\text{neigh}}m_{\text{SPH}} \lesssim 1 M_\odot \) for the simulation. Here \( N_{\text{neigh}} = 32 \) is the number of particles used in the SPH smoothing kernel (Bate & Burkert 1997).

The initial conditions for the second set of simulations (henceforth referred to as Halo 2) are derived from the simulations described in Stacy & Bromm (2013). These simulations were initialised at \( z = 100 \) in a 1.4 comoving Mpc box in accordance with the same ΛCDM structure formation model as Halo 1, but with \( \sigma_8 = 0.9 \) rather than the artificially enhanced \( \sigma_8 = 1.4 \) used in Halo 1. The use of ‘marker sinks’ for regions reaching densities beyond \( n = 10^3 \text{ cm}^{-3} \) rather than following the gas to higher densities allows for the efficient identification of the first 10 minihaloes to form within the box; we select the final minihalo to form—i.e., Minihalo 10 from Stacy & Bromm (2013)—for further study. After identifying the location of the final minihalo, the cosmological box is re-initialised at \( z = 100 \) using a standard zoom-in technique with two nested levels of refinement used to improve resolution surrounding the selected minihalo. Each ‘parent’ particle within the most refined region is split into 64 ‘child’ particles, with a minimum mass of \( m_{\text{gas}} = 1.85 M_\odot \) and \( m_{\text{PM}} = 12 M_\odot \). These refined simulations are then run until the gas approaches the typical onset of runaway collapse at \( n = 10^8 \text{ cm}^{-3} \).

3.1.1 Halo 2 Cut-out and Refinement

Once the simulation reaches \( 10^4 \text{ cm}^{-3} \) all particles beyond 10 comoving kpc from the centre of the collapsing minihalo are removed to conserve computational resources. To achieve a maximum resolution comparable to Halo 1, all particles within the 10 comoving kpc volume are split into two child particles placed randomly within the smoothing kernel of the parent particle. This particle-splitting is repeated twice more; all particles within 8 comoving kpc are replaced by 8 child particles; within 6 comoving kpc, each of these child particles is split into an additional 8 for a total of 128 child particles in the most refined region. At each step, the mass of the parent particle is evenly divided among the child particles and the smoothing length is set to \( hN_{\text{new}}^{1/3} \), where \( h \) is the smoothing length of the parent and \( N_{\text{new}} \) is the number of child particles created. All particles inherit the same entropy, velocity, and chemical abundances as their parent, ensuring conservation of mass, internal energy, and momentum.

While our cut-out technique leads to a rarefaction wave propagating inward from the suddenly introduced vacuum boundary condition, the average sound speed at the edge of the most refined region is \( \sim 0.5 \text{ km s}^{-1} \). As a result the wave only travels \( \sim 0.5 \text{ pc} \) over the remaining 400,000 yr of the simulation, a negligible fraction of the \( \sim 350 \text{ pc} \) physical box size.

3.2 Chemistry and Thermodynamics

We employ the chemistry network described in detail by Greif et al. (2009), which follows the abundance evolution of \( \text{H}, \text{H}^+, \text{H}^-, \text{H}_2, \text{H}_2^+, \text{He}, \text{He}^+, \text{He}^{++}, \text{D}, \text{D}^+, \text{HD} \) and \( \text{e}^- \). All relevant cooling mechanisms are accounted for, including H and He collisional excitation and ionisation, recombination, bremsstrahlung and inverse Compton scattering.

In order to properly model the chemical evolution at high densities, \( \text{H}_2 \) cooling induced by collisions with H and He atoms and other \( \text{H}_2 \) molecules is also included. Three-body reactions involving \( \text{H}_2 \) become important above \( n \gtrsim 10^8 \text{ cm}^{-3} \); we employ the intermediate rate from Palla et al. (1983), but see Turk et al. (2011) for a discussion of the uncertainty of these rates. In addition, the efficiency of \( \text{H}_2 \) cooling is reduced above \( \sim 10^9 \text{ cm}^{-3} \) as the ro-vibrational lines of \( \text{H}_2 \) become optically thick above this density. To account for this we employ the Sobolev approximation to.
3.3 Cosmic Ray Ionisation and Heating

Each time a CR proton ionises a hydrogen atom, an electron with average energy \( E = 35 \text{ eV} \) is produced (Spitzer & Tomasko 1964). Including the ionization energy of 13.6 eV, the CR proton loses approximately 50 eV per scattering. This necessarily places a limit on how many scatterings a CR proton can undergo before losing all its energy to ionisation, as well as limiting the distance it may travel. This distance may be described by a penetration depth

\[
D_p(n, \epsilon) \approx \frac{\beta c e}{-(d\epsilon/dt)_\text{ion}}
\]

where (Schlickeiser 2002)

\[
-(d\epsilon/dt)_\text{ion} \approx 1.82 \times 10^{-7} \text{ eV s}^{-1} n_H f(\epsilon),
\]

\[
f(\epsilon) = (1 + 0.0185 \ln(\beta)) \frac{2\beta^2}{\beta_0^2 + 2\beta^3},
\]

and

\[
\beta = \sqrt{1 - \left(\frac{\epsilon}{m_H c^2} + 1\right)^{-2}}.
\]

Here, \((d\epsilon/dt)_\text{ion}\) is the rate at which a CR proton loses energy to ionisation, \(\beta_0\) is the cutoff below which the interaction between CRs and the gas decreases sharply; we use \(\beta_0 = 0.01\), appropriate for CRs travelling through a neutral IGM (Stacy & Bromm 2007). As \(D_p(n, \epsilon)\) is the mean free path of CRs of energy \(\epsilon\) travelling through a gas with number density \(n\), we may define an effective cross-section \(\sigma_{CR}(n, \epsilon)\) for the interaction

\[
\sigma_{CR}(n, \epsilon) = \frac{1}{n D_p(n, \epsilon)}.
\]

As the CR penetration depth is \(\gg\) than the box size everywhere except approximating the centre of the star-forming minihalo, we may estimate the column density \(N\) —and thus, the CR attenuation along a given line of sight—using the same technique described in Hummel et al. (2015). The gas column density approaching the centre of the accretion disk varies by roughly an order of magnitude between the polar \((N_{\text{pole}})\) and equatorial \((N_{\text{equator}})\) directions, with the column density along these lines of sight well fit by

\[
\log_{10}(N_{\text{pole}}) = 0.5323 \log_{10}(n) + 19.64
\]

and

\[
\log_{10}(N_{\text{equator}}) = 0.6262 \log_{10}(n) + 19.57,
\]

respectively. We assume every line of sight within 45 degrees of the pole experiences column density \(N_{\text{pole}}\), while every other line of sight experiences \(N_{\text{equator}}\) (Hosokawa et al. 2011), allowing us to calculate an effective optical depth such that

\[
\epsilon^{-\tau_{CR}} = \frac{2\Omega_{\text{pole}}}{4\pi} e^{-\sigma_{CR} N_{\text{pole}}} + \frac{4\pi - 2\Omega_{\text{pole}}}{4\pi} e^{-\sigma_{CR} N_{\text{equator}}},
\]

where

\[
\Omega_{\text{pole}} = 2\pi \int_0^{\pi/4} \sin \theta d\theta = 1.84 \text{ sr}.
\]

Figure 2. Ionisation and heating rates as a function of total gas number density for both a cosmic ray and an X-ray background at \(z = 25\). In both panels, the solid blue lines denote the rate for our fiducial CR background, \(\rho_0\). The solid red lines show the fiducial X-ray rates from Hummel et al. (2015), while the dashed grey lines demonstrate the expected rates in the absence of gas self-shielding. The dash-dotted blue (red) lines mark the highest-intensity CR (X-ray) heating and ionisation rates investigated. For a given energy density, CRs are more effective at ionising and heating the gas; vertical placement on this chart is simply a matter of normalisation, stemming from the assumptions outlined in Section 2. Note that X-rays cause significantly more heating per ionisation event than CRs, but are strongly attenuated at high densities. CRs are significantly more penetrative in comparison.

Accounting for this attenuation of the CR background and following the treatment of Stacy & Bromm (2007) and Inayoshi & Omukai (2011), the cosmic ray heating rate \(\Gamma_{CR}\) and ionisation rate \(k_{CR}\) are given by

\[
\Gamma_{CR} = \frac{E_{heat}}{50 \text{ eV}} \int_{\epsilon_{min}}^{\epsilon_{max}} \left| \frac{d\epsilon}{dt} \right| \frac{d n_{CR}}{d\epsilon} e^{-\tau_{CR}} d\epsilon,
\]

and

\[
k_{CR} = \frac{\Gamma_{CR}}{n_H E_{heat}},
\]

where \(\epsilon_{min} = 10^6 \text{ eV}, \epsilon_{max} = 10^{15} \text{ eV}, n_H\) is the number density of hydrogen, and \(E_{heat}\) is the energy deposited as heat per interaction (Schlickeiser 2002). While CRs lose about 50 eV per interaction, only about 6 eV of that goes towards heating in a neutral medium (Spitzer & Scott 1969; Shull & van Steenberg 1985): we set \(E_{heat}\) accordingly.

Here we assume the incident CR background is composed solely of protons, and all interactions occur with hydrogen only. While this neglects the slight difference in average CR energy loss per interaction for hydrogen (36 eV;...
Our sink particle method is described in [Stacy et al., 2010]. When a gas particle exceeds $n_{\text{max}} = 10^{12} \text{cm}^{-3}$, it and all non-rotationally-supported particles within the accretion radius $r_{\text{acc}}$ are replaced by a single sink particle. We set $r_{\text{acc}}$ equal to the resolution length of the simulation: $r_{\text{acc}} = L_{\text{res}} \approx 50 \text{ AU}$, where

$$L_{\text{res}} \approx 0.5 \left( \frac{M_{\text{res}}}{\rho_{\text{max}}} \right)^{1/3},$$

and $\rho_{\text{max}} = n_{\text{max}} m_\text{H}$. Upon creation, the sink immediately accretes the majority of the particles within its smoothing kernel, resulting in an initial mass for the sink particle $M_{\text{sink}}$ close to $M_{\text{res}} \approx 1 \text{ M}_\odot$. Following its creation, the density, temperature, and chemical abundances of the sink particle

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**Figure 3.** Mass-weighted temperature-density distribution of the gas collapsing into Halo 1 (top) and Halo 2 (bottom), shown just prior to sink formation. Each panel shows the behaviour of gas collapsing under a CR background of a given strength. In each case, the behaviour of the gas in the $u_{\text{CR}} = 0$ case is reproduced for comparison (light grey); dashed lines denote the CMB temperature when collapse occurs. Gas at low densities gets progressively hotter and gas in the loitering phase gets progressively cooler with increasing $u_{\text{CR}}$. Note that the gas invariably proceeds to collapse, and converges toward a similar thermodynamic path as it approaches sink formation densities, regardless of the CR background strength.

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Bakker & Segrè 1951 as compared to helium (40 eV; Weiss & Bernstein 1956), the resulting error in the employed heating and ionisation rates is sufficiently small for our purposes (see Jasche et al. 2007 for a more rigorous treatment).

The resulting heating and ionisation rates for both the $u_{\text{CR}} = u_0$ and $10^2 u_0$ cases are shown in Figure 2 along with the expected rates in the absence of attenuation. Also shown are the highest and lowest X-ray heating and ionisation rates considered in [Hummel et al., 2015]. Compared to X-rays, CRs produce significantly less heating per ionisation event and penetrate to much higher densities before being attenuated; the X-ray heating and ionisation rates fall off much faster as the gas becomes optically thick.
4 RESULTS

4.1 Initial Collapse

4.1.1 CR-enhanced H₂ Cooling

The gas in both Halo 1 and Halo 2 invariably collapses to high densities, even as we vary the CR background strength by five orders of magnitude. As seen in Figure 3, the collapse occurs in accordance with the standard picture of Pop III star formation (e.g., Greif et al. 2012; Stacy & Bromm 2013; Hirano et al. 2014; Hosokawa et al. 2015), albeit slightly modified by the presence of a CR background. In each case, the gas heats adiabatically as it collapses until reaching \( \sim 10^3 \text{K} \), at which point H₂ cooling is activated. This allows the gas to cool to \( \sim 200 \text{K} \), whereupon it enters a 'loitering' phase (Bromm et al. 2002), increasing in density quasi-hydrostatically until sufficient mass accumulates to trigger the Jeans instability, typically between \( 10^4 \text{cm}^{-3} \) and \( 10^6 \text{cm}^{-3} \). Runaway collapse then proceeds until three-body reactions become important at \( n \sim 10^8 \text{cm}^{-3} \); this turns the gas fully molecular by \( n \sim 10^{12} \text{cm}^{-3} \), at which point we insert sink particles.

As demonstrated in Figure 4, increasing \( u_{\text{CR}} \) both heats the gas and boosts the resulting ionisation fraction. This in turn increases the efficiency of H₂ formation, enhancing cooling and allowing gas in the loitering phase to reach progressively lower temperatures. In fact, the additional cooling is sufficient to cool the gas all the way to the CMB floor when \( u_{\text{CR}} \gtrsim 10^4 u_0 \). However as the gas exits the loitering phase and proceeds to higher densities, the CR optical depth increases significantly. In concert with the onset of three-body processes this renders CR ionisation and heating ineffective at high densities. As a result, the thermal behaviour of the gas increasingly resembles that seen in the \( u_{\text{CR}} = 0 \) case as the collapse proceeds. To wit, by the time we form sink particles at \( 10^{12} \text{cm}^{-3} \) the thermodynamic state of the gas is remarkably similar, even as we vary the CR background strength by five orders of magnitude. This convergence under a wide range of environmental conditions is similar to that seen in the presence of both an X-ray background (Hummel et al. 2015) and DM–baryon streaming (Stacy et al. 2011; Greif et al. 2011b).
Figure 6. Simulation structure for both Halo 1 (top) and Halo 2 (bottom) as seen in the final output, 5000 yr after the first sink forms. Shown is a density projection of the minihalo environment on progressively smaller scales for both the $u_{\text{CR}} = 0$ and $u_{\text{CR}} = 10^5 u_0$ simulations, as labelled. White boxes indicate the region depicted on the next smaller scale. From left to right: filamentary structure of the cosmic web near the minihalo formation site; minihalo formation at the intersection of several filaments; morphology within the $\sim 100$ pc virial radius of the minihalo. The density scale for each level is shown just to the right – note that the scaling changes from panel to panel. Note how the gas in the $u_{\text{CR}} = 10^5 u_0$ simulations appears smoothed out compared to the $u_{\text{CR}} = 0$ simulations. Not only do CRs heat and smooth the filamentary gas, the expedited collapse induced by CR ionisation leaves less time for low-density structure to form, since the collapse is shifted to an earlier epoch. As a result, the dynamical environment in which the sink particles form varies significantly between simulations.
4.1.2 Expedited Collapse

Boosting the H$_2$ fraction in the gas lowers the density threshold for efficient cooling, allowing the gas to fulfill the Rees-Ostriker criterion sooner by driving the cooling time $t_{cool}$ below the freefall time $t_{ff}$ \cite{Rees1977}. This is demonstrated in Figure 6 where we see the density at which the gas begins to cool drop as the CR background strength increases. This necessarily expedites the subsequent phases of the collapse, as seen clearly in Figure 5 where we show the total gas mass within 1 pc (physical) of the minihalo’s centre as a function of redshift. The impact this has on the environment in which the minihalo collapses is seen in Figure 6 where we show the final simulation output on various scales for Halo 1 and Halo 2, both in the absence of any CR background ($u_{CR} = 0$) and with $u_{CR} = 10^5 u_0$. Low density filamentary gas is heated and prevented from collapsing, reducing the clumping of the IGM and possibly impacting the early stages of reionisation. Gas above a $u_{CR}$-dependent density threshold on the other hand experiences enhanced cooling and thus has its collapse expedited. As a result, the dynamical environment in which the first sink particles form varies significantly depending on the strength of the CR background.

4.2 Star Formation

4.2.1 Protostellar Fragmentation and Growth

Figure 7 shows the growth over time of all sink particles formed in our simulations, from formation of the first sink particle to simulation’s end 5000 yr later when radiative feedback can no longer be ignored. The first sink particle forms when the gas in the centre of the minihalo reaches densities of $10^{12}$ cm$^{-3}$, and develops an accretion disk within a few hundred years. In all but three cases, this disk quickly fragments, forming a binary or small multiple within 500 yr. Sinks that survive longer than a few hundred years without undergoing a merger quickly accrete the surrounding gas, growing to $\sim$ a few solar masses within 500 yr and typically reaching between 10 and 40 M$_\odot$ by simulation’s end.

As is evident from Figure 7, there is no clear trend with $u_{CR}$ in either protostellar growth or accretion rate, nor is there any trend in the total sink mass. For example, both the $10 u_0$ Halo 1 simulation and $10^5 u_0$ Halo 2 simulation form only a single sink while the $10^3 u_0$ Halo 2 simulation steadily forms a total of 14 sink particles over the 5000 yr period. This can be primarily attributed to the wide variety of dynamical environments in which the sink particles form—demonstrated in Figure 8 where we show the accretion disk structure of each simulation 5000 yr after the
first sink formed. This variation is a direct consequence of the expedited collapse discussed in Section 4.1.2. As seen in Figure 6, expediting the initial collapse results in significant variation of the experienced gravitational potential; the collapse history of the gas and the dynamical environment in which the sinks form varies accordingly. Given the lack of any apparent trends with increasing $u_{\text{CR}}$, this suggests the final stages of the collapse are influenced more by small-scale turbulence than the strength of the CR background. While CRs may indeed alter the susceptibility of the disk to fragmentation, any such behaviour is masked by variations in the collapse history between simulations.

### 4.2.2 Characteristic Mass

While the final stages of the collapse appear to be somewhat chaotic, with protostellar fragmentation driven primarily by small-scale turbulence rather than the CR background, the typical mass of the sinks formed remains quite stable across all simulations at $10^{-4} - 40 \, M_\odot$. This is very much in line with the prevailing consensus for the expected mass of the first stars in the absence of any radiative feedback of $\sim$ a few $\times 10 \, M_\odot$ (Bromm 2013). As noted in Section 4.1.1, the thermodynamic behaviour of the gas displays a remarkable similarity as it approaches sink formation densities, regardless of $u_{\text{CR}}$. This suggests that the influence of the CR background is restricted to lower densities, with little to no effect on the protostellar cores from which the first stars ultimately form.

The universality of this characteristic mass is further supported by Figure 9, where we show the average gas temperature as a function of number density, as well as the approximate fragmentation mass scale, as estimated by the
Bonnor-Ebert mass (e.g., Stacy & Bromm 2007):

\[ M_{\text{BE}} = 700 \, M_\odot \left( \frac{T}{200 \, \text{K}} \right)^{3/2} \left( \frac{n}{10^4 \, \text{cm}^{-3}} \right)^{-1/2} \], \quad (19)

where \( n \) and \( T \) are the number density and corresponding average temperature. Approaching sink formation densities \( M_{\text{BE}} \) is nearly independent of \( u_{\text{CR}} \), in agreement with the observed lack of evolution in the sink mass.

Also shown in Figure 9 are the one-zone calculations from Stacy & Bromm (2007). Investigating the impact of a CR background on Pop III star formation in a \( z = 21 \) minihalo using the CR background strengths shown in Figure 1, their models suggested that a sufficiently strong background might decrease the fragmentation mass scale by an order of magnitude as a result of the cooler temperatures experienced during the loitering phase. While we observe similar behaviour from gas in the loitering phase, once the gas proceeds to runaway collapse its thermodynamic state quickly converges with that of the \( u_{\text{CR}} = 0 \) case, such that the fragmentation mass scale remains unaltered. Unfortunately the models of Stacy & Bromm (2007) only followed the gas evolution up to densities of \( 10^6 \, \text{cm}^{-3} \), insufficient to observe this convergent behaviour.

5 SUMMARY AND CONCLUSIONS

We have performed two suites of cosmological simulations employing a range of CR backgrounds spanning five orders of magnitude in energy density. We follow the thermodynamic evolution of the gas as it collapses into a minihalo from IGM densities up to \( n = 10^{12} \, \text{cm}^{-3} \), at which point three-body processes have turned the gas fully molecular. This allows us to capture the combined impact of CR heating and ionisation on Pop III stars forming in the minihalo via its influence on H\(_2\) and HD cooling. Once the gas reaches \( n = 10^{12} \, \text{cm}^{-3} \), we form sink particles and follow the subsequent evolution of the system for \( 5000 \) yr, after which point radiative feedback from the forming protostars can no longer be ignored, and our simulations are terminated.

While it also serves to heat the gas, the primary impact of the CR background is to increase the number of free electrons in the collapsing gas, catalysing the formation of additional molecular hydrogen, which in turn enhances the H\(_2\) cooling efficiency. This decreases the cooling time, allowing the gas to fulfil the Rees-Ostriker criterion sooner and expediting minihalo collapse. Each simulation therefore collapses to high density at a different epoch, and the resulting variation in experienced gravitational potential causes the collapse history—and thus the accretion disk structure—to differ greatly between simulations.
Our first suite of simulations (Halo 1) used the same initial conditions as our prior investigation of a cosmic X-ray background (Hummel et al. 2015), allowing for a direct comparison of the results. CRs are much less efficient than X-rays at heating the gas, such that the collapse suppression observed for a sufficiently strong X-ray background does not occur here. While expedited collapse is observed in the presence of an X-ray background as well, the effect is somewhat more pronounced here owing to the more efficient nature of CR ionisation, as there is less associated heating to partially counteract the enhanced cooling.

Our second suite of simulations focused on a minihalo collapsing at $z \simeq 21.5$ in the $u_{\text{CR}} = 0$ case in order to allow a more direct comparison to the results of Stacy & Bromm (2007), and control for the influence of the CMB temperature floor on our results. While we find similar evidence for a lower gas temperature in the loitering phase, extending our study beyond the $n = 10^6 \text{ cm}^{-3}$ limit of Stacy & Bromm (2007) revealed that the thermodynamic path of the collapsing gas—and thus, the fragmentation mass scale—begins to converge with that of the $u_{\text{CR}} = 0$ case for $n \gtrsim 10^6 \text{ cm}^{-3}$. This convergence is observed in all simulations for both Halo 1 and Halo 2, with the thermodynamic state of the gas becoming nearly independent of $u_{\text{CR}}$ at the time we form sink particles at $n = 10^{12} \text{ cm}^{-3}$. The remarkable similarity in the thermodynamic state of the gas just prior to sink formation suggests the presence of a CR background has little impact on the characteristic mass of the stars formed. Indeed, the typical mass of the sink particles formed is quite robust, remaining stable across all simulations at $10 - 40 M_\odot$, very much in line with the expected mass of the first stars in the absence of external radiative feedback. In fact, this robust behaviour is observed under a variety of environmental conditions, including X-ray irradiation (Hummel et al. 2015) and DM–baryon streaming (Stacy et al. 2011) by Greif et al. 2011b).

While the neutral impact of the CR background on the thermodynamic state of primordial gas at high densities results in a robust characteristic mass that does not vary with $u_{\text{CR}}$, there is a possibility that the enhanced cooling resulting from CR ionisation may decrease the velocity dispersion of the infalling gas (Clark et al. 2011a). This would decrease fragmentation in the centre of the minihalo, possibly increasing the mass of the stars formed. While we see no evidence to support this, any such systematic effect could be easily masked by the variations in collapse history between simulations. Likewise, the fact that each simulation collapses to high densities at a different epoch in a different gravitational potential well limits our ability to draw detailed conclusions regarding the impact of the CR background on fragmentation in the protostellar accretion disc.

Finally, while the characteristic mass—and thus, ionising output—of Pop III stars appears to be unaffected by the presence of a CR background, CRs still heat the low-density gas in the IGM, reducing its clumping factor. This may have implications for reionisation and the 21-cm signal (Furlanetto et al. 2006; Sazonov & Sunyaev 2015).

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