Tunability of Interactions between the Core and Shell in Rattle-Type Particles Studied with Liquid-Cell Electron Microscopy

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ABSTRACT: Yolk−shell or rattle-type particles consist of a core particle that is free to move inside a thin shell. A stable core with a fully accessible surface is of interest in fields such as catalysis and sensing. However, the stability of a charged nanoparticle core within the cavity of a charged thin shell remains largely unexplored. Liquid-cell (scanning) transmission electron microscopy is an ideal technique to probe the core−shell interactions at nanometer spatial resolution. Here, we show by means of calculations and experiments that these interactions are highly tunable. We found that in dilute solutions adding a monovalent salt led to stronger confinement of the core to the middle of the geometry. In deionized water, the Debye length $\kappa^{-1}$ becomes comparable to the shell radius $R_{\text{shell}}$, leading to a less steep electric potential gradient and a reduced core−shell interaction, which can be detrimental to the stability of nanorattles. For a salt concentration range of 0.5−250 mM, the repulsion was relatively long-ranged due to the concave geometry of the shell. At salt concentrations of 100 and 250 mM, the core was found to move almost exclusively near the shell wall, which can be due to hydrodynamics, a secondary minimum in the interaction potential, or a combination of both. The possibility of imaging nanoparticles inside shells at high spatial resolution with liquid-cell electron microscopy makes rattle particles a powerful experimental model system to learn about nanoparticle interactions. Additionally, our results highlight the possibilities for manipulating the interactions between core and shell that could be used in future applications.

KEYWORDS: rattle particles, yolk−shell, nanoparticles, liquid-cell electron microscopy, electrical double layer, electrostatic interactions
interactions for nanoscale objects are effective at a length scale of nanometers to hundreds of nanometers. Therefore, any technique used to investigate the interaction potential of such objects needs to have nanometer spatial resolution. Other studies have shown that it is possible to infer an interaction potential from observations made with liquid-cell electron microscopy, even if those particles were trapped near the surface of the liquid-cell geometry.12,13,15,16 Additionally, the flow-through capability of the liquid-cell holder allows control over essential solution parameters such as pH and ionic strength in situ and makes it possible to observe direct changes in the interaction potential and the colloidal stability of the core particle within a shell when the shell is adsorbed to one of the windows of the liquid cell.

The interaction between spherical charged colloidal particles dispersed in a liquid is an extremely well-studied topic within colloid science,18–62 and here is certainly not the place to review this topic in any depth.39–45 Understanding the interactions between colloidal particles is not only of importance to almost all applications in which colloids are used but has over the last century also become an important topic in “multiple-particle” statistical physics where one of the goals is to derive effective potentials from a lower-level description.45–48 The description of the interactions between charged spheres that is most often used in theoretical and experimental studies is referred to as the DLVO potential. DLVO refers to Derjaguin, Landau, Verwey, and Overbeek, who were the principle investigators that developed the theoretical framework to describe these interactions, mostly in the 1940s.36–39 It may come as a surprise that the strongly related topics of the dynamics and interactions of a spherical particle that is present inside a liquid-filled spherical shell are much less well studied63,64 despite the already mentioned recent progress in realizing such systems. This lack of knowledge is, for instance, illustrated by a recent paper which was the first to theoretically describe the dynamics of a single charged colloidal particle between two flat, confining walls where the range of the double layer repulsion and the distances between the walls are similar.60 It should additionally be remarked that this flat-plate geometry of the confinement is significantly simpler than that of a spherical particle inside a spherical shell.46,47 The reason for the absence of theoretical studies is almost certainly due to a lack of experimental studies in which accurate local dynamics and/or interaction potentials under similar confining geometries have been measured. There is also a strong need for experimental studies on the more-or-less direct measurements of colloid—colloid interaction potentials for nanoparticles (NPs). The reason for the lack of studies is, besides the necessarily higher spatial resolution needed and much smaller volume of the NPs, additional experimental difficulties. For example, optical tweezers cannot be used to measure NP interactions50,56 because ion transport through the shell from the outside liquid to the inside and vice versa. However, this speed with which ion transport through the shell occurs with regard to the dynamics of the moving core particles is usually significantly lower than that of the ions freely diffusing in the liquid, thus possibly undermining certain assumptions made in the theoretical description. The dynamics of the ions going through the shell is not characterized in the present work as well and is left for future work. Additionally, even without the charge-induced interactions, a diffusing particle inside a hollow shell already has a complex position-dependent mobility because of the boundary conditions of the hydrodynamics.46,47,50,54 The coupling between the interactions and the hydrodynamics only complicates this further.46 However, this involved position dependence also holds promise, as it can be used to locally measure the temperature and/or ionic strength if the dynamics of the ions and interactions with the shells are sufficiently well understood theoretically and controlled experimentally. Moreover, it is
clear from the information above that this geometry as it already can be studied in a liquid-cell by high-resolution imaging is also a powerful experimental model system to learn about interactions of nanoparticles in 3D in different solvents, including water for the first time in experiments.

RESULTS AND DISCUSSION

In this study, we imaged rattle-type particles in water while changing the salt concentration in situ. We investigated two kinds of rattle-type particles (Figure 1). The first kind are composed of a sub-micrometer-sized titania core and a silica shell (Figure 1a), which were made by removing a polystyrene sacrificial layer by calcination. They are promising building blocks for optical colloidal crystals because the locations of cores in the shell compartment can be reversibly controlled using external stimuli. The second kind are nanorattles consisting of a gold nanoparticle in a silica shell (Figure 1b), synthesized by a surface-protected etching process that removes a sacrificial silica layer, and are promising materials for sensing. The diameter of the core, inner diameter of the shell, and the thickness of the shell, as well as the zeta-potential of the core particle, are reported in Table 1. Details of the synthesis procedure can be found in the Supporting Information and previous work by Watanabe and co-workers.

Table 1. Measured Quantities of the Two Types of Rattles Used in This Work: Core Radius Rcore, Inner Shell Radius Rshell, Inner Shell Thickness Tshell, and Zeta-Potential of the Core ζcore

| particle            | Rcore (nm) | Rshell, Inner (nm) | Tshell (nm) | ζcore (mV) |
|---------------------|------------|--------------------|-------------|------------|
| titania@void@silica | 165 ± 18   | 357 ± 24           | 27 ± 2      | −54 ± 1    |
| gold@void@silica    | 17 ± 2     | 86 ± 5             | 5 ± 1       | −50 ± 4    |

The zeta-potential of the core particle was measured in aqueous solution at a pH of 7 and an ionic strength of 1.00 mM LiCl salt.

In short, the rattle-type particles were investigated using liquid-cell scanning transmission electron microscopy (LC-STEM). The dispersion of rattles in water was drop-cast onto a glow-discharged Si microchip in a dedicated holder, and a second Si microchip was placed on the bottom chip. The closed holder was introduced into the microscope, and deionized water was flowed through the liquid cell at a rate of 2 μL/min for 45 min. The flow was turned off for imaging of the moving core particle inside a shell that was attached to the electron-transparent window of the liquid cell. Subsequently, a new LiCl concentration was flowed into the shell at a rate of 2 μL/min for 15 min. The moving core particle was then imaged again with the flow turned off. This procedure was repeated for all salt concentrations. Typical resulting images for the titania@water@silica rattles in 0.500 and 25.0 mM LiCl (aq) with a frame time of 1 s are shown in Figure 2a. Due to the high mobility of the core particle in water, the particle could not be tracked directly. Using the analysis outlined in Figure 2b, a measure of the probability of finding the particle at certain positions within the shell was obtained. We filtered the intensity from the core particle of every single frame and averaged those in a single image. We then corrected for the available volume in the z direction (Supporting Information) and deconvoluted with a simulated image of a titania particle to obtain a projected probability map of finding the particle in a certain position within the projected shell. Details of the data acquisition and image simulation and processing are given in the Methods section.

Before results can be interpreted, as in any experiment involving liquid-cell electron microscopy, the influence of the electron beam has to be investigated. Figure 3 shows images of the maximum intensity of all pixels throughout the whole image series for a titania core exploring a silica shell. This effectively visualizes how close the core particle was able to approach the shell throughout the complete image series. It is evident that the core particle approached the shell more closely at higher electron dose rates. This means that the electron beam influenced the interactions between the titania particle and the silica shell. Earlier studies have observed changes in the interactions between NPs in liquid-cell scanning transmission electron microscopy (LC-STEM) and argued they could be caused by either a change in pH or a change in the ionic strength. A significant change in the local temperature is not expected at these electron dose rates. We used different electron dose rates to investigate titania@water@silica rattle particles in deionized water and in 10.0 mM LiCl in order to distinguish between the pH or the ionic strength being influenced by the electron beam irradiation. We observed that a similar decrease in minimum distance of approach to the shell for increasing electron dose rates occurred in deionized water and 10.0 mM LiCl (Figure 3). From this, we infer that the change in ionic strength is not the main contributing factor in our system. We believe the change in the core–shell interaction can be explained by taking into account a change in pH due to electron–water interactions. As more H2O+ than OH− is produced, the pH drops when water is irradiated with the electron beam. It is well-known that both titania and silica lose charge when the pH drops. Additional experiments on how the influence of the electron beam seems related to pH can be found in the Supporting Information. We performed our subsequent experiments for titania@water@silica rattles at a moderate dose rate of 45 e− nm−2 s−1 to overcome the change of interaction at high dose rate, while obtaining an acceptable signal-to-noise ratio. For this dose rate, the decrease in range of the repulsive interactions due to the electron beam is likely to be only a few nanometers, while the range of interactions for which we extract interaction potentials in this work is 15–100 nm. Interactions within a Titania@water@silica Rattle-Type Particle. Having determined the influence of the electron beam, we next aimed to investigate the influence of the ionic strength on the interaction potential between a titania core and a silica shell (Supporting Movie S6). The salt we used
was LiCl, as these (solvated) ions most likely diffuse through the porous silica shells.73 Figure 4 shows the influence of the salt concentration on the relative projected probability of finding the titania particle as a function of its position within the shell in the microscopy images, which are 2D projections of a 3D system. In Figure 4a, the projected probability maps for all salt concentrations are given for a single rattle-type particle. Figure 4b,c shows the projected probability as a function of the projected core-to-shell distance, which is the distance between the surfaces of the core and the inner shell as observed in the 2D microscopy images. The projected probability for a particle in low salt concentrations in Figure 4b was fitted to a 3D interaction potential, resulting in Figure 4d. In short, we assumed a perfectly spherical rattle geometry and used the relation between the interaction potential $U(r)$ and probability $P(r)$ to find a particle at a certain radial position:

$$\frac{U(r)}{k_B T} = -\ln(P(r))$$

(1)

Projecting a probability derived from a trial potential, $U_{\text{trial}} = A \frac{e^{-r}}{r}$, with $\kappa$ (the inverse Debye length) and $A$ as fitting parameters, and fitting this to the experimental projected probability of finding the core at a certain radial position allowed us to find a 3D experimental interaction potential, which is eventually expressed as a function of particle-shell distance $d$. Additional details can be found in the Methods section and Supporting Information. This fitting procedure was not performed for the projected probability for a particle in high salt concentrations in Figure 4c, as the origin of the high projected probability close to the projected shell is uncertain, as will be discussed later. Finally, Figure 4e shows the results of finite-element calculations for a rattle geometry solving the nonlinearized Poisson–Boltzmann equation for a symmetric 1:1 electrolyte:

$$-\varepsilon_0 \varepsilon_i \nabla^2 \psi = 2 \varepsilon_0 \sinh \left( \frac{eV}{k_B T} \right)$$

(2)

Here, $\psi$ is the electric potential, $\varepsilon_0$ is the permittivity of vacuum, $\varepsilon_i$ is the dielectric constant of the liquid, $\varepsilon_0$ is the salt concentration, $e$ is the electron charge, $k_B$ is the Boltzmann constant, and $T$ is the temperature. On the surface of the core and the shell, we assumed constant surface potential boundary conditions.
Three interesting points arise from Figure 4. First, the electrostatic repulsion had a longer range than expected for sphere−sphere interactions. Second, when no salt is added, the titania particle approached the shell more closely than when 0.500 or 1.00 mM LiCl was added, even though the Debye screening length is significantly longer in deionized water. Third, the titania particle remained colloidally stable within the shell up to 250 mM LiCl and was found to be more often close to the shell than in the middle of the geometry. We discuss these three phenomena in the following sections.

First, let us turn to the long-ranged electrostatic interaction between a sphere and a shell. The experimental interaction potentials are less steep than the calculated potentials, which is likely due to experimental limitations such as resolution. Using the equations outlined in the work of de Jonge,31 we estimate the resolution in our experimental data to be approximately 11.6 nm in our experiments with titania@water@silica rattle-type particles (Supporting Information). Errors in the determination of the interactions between the core and shell mostly stem from resolution and the 2D projection of a 3D system. The resolution likely leads to errors in determining the projected core−shell distance and to less steep interaction potentials. The 2D projected data lead to a lower accuracy of the projected probability when the particle is near the projected shell wall. Despite the errors in the experimental data it shows the same trends as the calculations and the long-ranged character of the interaction potential is present for both the experiments and the calculations. To get more insight in this long-ranged repulsion, we calculated the electrostatic interaction for both a sphere−sphere system and a sphere−shell system using a finite-element method to solve the nonlinear Poisson−Boltzmann equation with constant surface potential.

Figure 4. Influence of the salt concentration on the interactions between the titania core and the silica shell in a titania@water@silica rattle-type particle. (a) Projected probability maps of finding the core particle in a certain part of the projected shell. The dashed circles show the projected area available to the particle in the shell. The scale bar indicates 100 nm. (b,c) Projected probabilities of finding the particle a projected distance away from the shell wall at various salt concentrations. The projected probabilities for each concentration were averaged over three different particles. The relative projected probability to find the core particle in the center of the shell was set to 1. The relative projected probabilities for individual particles are shown in Figure S11. (d) 3D interaction potentials obtained from the fits in b. (e) Electrostatic interaction potentials calculated by solving the nonlinear Poisson−Boltzmann equations with constant surface potential using a finite-element method for a core particle with radius $R_{\text{core}} = 170$ nm and surface potential $\psi_{\text{core}} = -50$ mV inside a shell with inner radius $R_{\text{shell}} = 350$ nm and inner surface potential $\psi_{\text{shell}} = -60$ mV.
approximately 65 nm for the sphere–sphere interaction, whereas it is approximately 82 nm for the sphere–shell interaction. This difference is more than one Debye length (for 0.5 mM, $\kappa^{-1} = 13.6$ nm), which is quite significant. In Figure 5c, it is shown that the potential from the surface of the inner shell wall (right-hand side of the plot) decays more slowly than that of a spherical particle; the difference is more pronounced when the core is off-center (Supporting Information). This is due to the concave geometry of the shell as found previously for hollow shells.74 This slow decay of the electric potential is the reason for the long-ranged interaction in a sphere–shell system. Furthermore, it is likely a reason why the core particle was stable at 250 mM concentration of LiCl.

Second, the apparently weak core–shell interaction in deionized water was investigated. In Figure 4b,d, it is shown that the core particle is less confined to the middle of the shell for deionized water compared to moderate amounts of salt in the solution (0.500 and 1.000 mM LiCl, respectively). Furthermore, the interaction potential in deionized water was less steep than that in moderate amounts of salt. In Figure 5d, we observe that the interaction in deionized water (we assume an ionic strength of 2 μM) for two spheres is in a range of the order of a micron. This range is much larger than the space available in the rattle geometry. As such complete double layer overlap cannot occur, the interaction between core and shell is significantly altered. Figure 6 explores this in more detail by comparing the calculated core–shell interaction in deionized water (ionic strength of 2 μM, $\kappa^{-1} = 215$ nm) with the interaction for an ionic strength of 0.5 mM ($\kappa^{-1} = 13.6$ nm). The interaction in 2 μM salt is significantly less steep than the interaction in 0.5 mM salt. Figure 6b shows that when the core particle is in the middle of the shell, the electric potential $\psi$ originating from the surfaces of the core and the shell decays to almost 0 in the middle between the two surfaces for an ionic strength of 0.5 mM. However, in deionized water, the electric potentials coming from both the surface of the core particle and the inner shell surface hardly decay. This leads to an almost flat electric potential within the entire shell geometry, significantly reducing the electrostatic interaction between the
core and shell. It is noteworthy that this phenomenon was found in water. As previously stated, due to the self-dissociation of water, it is difficult to reach ionic strengths lower than 1 \( \mu M \) and Debye lengths larger than 300 nm. The shell geometry helps significantly in this regard. The core particle cannot escape the shell and can only be a maximum distance away from the shell wall at all times. Furthermore, the slower decay of the electric potential from the inner shell surface means the electric potential is even more flat due to the rattle geometry.

Third, we discuss the interesting phenomenon at high ionic strength for which the core particle spends more time near the projected shell than in the middle of the rattle geometry (Figure 4c). One explanation is the presence of an attractive potential that the core experiences when it is close to the shell. The likelihood of van der Waals attractions is a good candidate for such attractions according to the calculations (Methods section) and as shown in Figure 5e, where the sphere–shell secondary minimum is more severe than the sphere–sphere secondary minimum. However, in our sphere–shell system, there was also an influence of hydrodynamic interactions when the core particle was near the shell wall. This slowed down the particle near the shell wall, similarly to how it would near a flat surface.\(^{46,75}\)

Therefore, we investigated how hydrodynamic slowing down of the core particle shows up in the analysis of our experimental microscopy data due to the finite time of our measurements. We are aware of the fact that in equilibrium statistical mechanics the effects of hydrodynamics cannot be part of a probability (density). However, because of the finite time of our measurements, hydrodynamic effects can and do show up. As these effects are not correctly taken into account, the probability function should then more correctly be labeled as "apparent probability density". To uncover how much hydrodynamic interactions influenced our experimental data, we simulated annular dark-field scanning transmission electron microscopy (ADF-STEM) images of a core particle diffusing within a shell. In short, for every time step (equal to the pixel dwell time), we let the particle (starting from a random position within the shell) move in a random direction according to the position-dependent and direction-dependent diffusion coefficient (Figure S5a). Knowing the position of the particle for the pixel that is currently being scanned, we took the weighted average value of that pixel for the three static simulated images of the rattle particle for which the position of the core particle best resembled the current position. This was done for all pixels in order to form an image of a moving core particle within a shell. We simulated 180 images per series, which is roughly the same amount as the number of images per salt concentration in the experiments. More details can be found in the Methods section. Figure 7a shows images resulting from this simulation for which the particle could move freely until it approached 120 or 60 nm from the shell wall, respectively (Figure 7b). The simulated images look similar to the experimental images shown in Figure 2a. In Figure 7c, the projected probabilities of finding the particle at a certain distance from the shell from simulated images are shown. We observed that when the particle was allowed to approach the shell closely, the projected probability of finding the core particle near the shell wall was higher than in the middle of the shell geometry. Since there was no attractive potential in our simulations, this was a direct consequence of the hydrodynamic slowing down of the core particle. It is thus likely that hydrodynamics effects contribute to the higher projected probability of finding the particle near the projected shell wall found in Figure 4c due to the finite time of our measurements. Both hydrodynamic effects and van der Waals attractions could lead to the increased probability of finding the core particle near the projected shell wall in our measurements. Since it was hard to distinguish between both

![Simulated images](https://doi.org/10.1021/acsnano.1c03140)
effects (Supporting Information), we did not attempt to extract the interaction potential at high salt concentrations.

However, when the particle was not allowed to move close to the shell wall, the effect of the hydrodynamics proved much more limited. Figure 7d gives a good impression of the systematic error that hydrodynamic interactions, but more importantly limited resolution, would induce on the potentials we extracted in Figure 4d for the cases of moderate salt concentrations (0.5–5 mM). Based on the magnitude of these apparent potentials, we are confident in our extracted interaction potentials in Figure 4d.

Interactions within a Gold@water@silica Nanorattle.
Lastly, the interactions between a gold nanosphere (R_{core} = 17 nm) and a thin silica shell (R_{shell} = 80 nm) were investigated in Figure 8. These particles can really be considered nanorattles and are so small that liquid-cell electron microscopy is the only technique that is able to obtain reliable real space information on them in water as a solvent. The electron dose rate in these measurements was 206 e⁻ nm⁻² s⁻¹. As found for the titania particle, the experimental interaction potentials are not as steep as the calculated potentials. However, this effect is less pronounced as the resolution is slightly better when imaging gold particles (7.8 nm) in comparison to titania cores (11.6 nm). Especially, the calculated and experimental interaction potentials for 2.00 and 5.00 mM LiCl agree excellently. Interestingly, the experimental potential for an ionic strength of 0.500 mM indicates a repulsion of longer range than the calculated interaction potential. This could be due to an underestimation of the surface potential in the calculations. For gold@water@silica rattles, similarly to the much larger titania@water@silica rattles, the core particle approached the shell more closely without any added salt, compared to the situation for 0.500 mM LiCl. Moreover, we observed many instances of the gold core particle getting stuck to the shell in pure water (Figure S13 and Movie S8). There are even instances where the particle got stuck to the shell in one frame and the electron beam enables it to move again to the next frame. The influence of the electron beam is hard to determine here, but the particle getting stuck to the shell only happens when no salt was added, which hints that the repulsion between the core and shell was lowest for this case. These results indicate that in these nanorattles flat electric potentials can be detrimental to the stability of the core particle within the shell, especially when the surfaces are not highly charged or when they are in a medium with a character less polar than that of water. It is therefore recommended to have some salt present in dispersions of nanorattles at all times if mobility of the core particle is desired.

CONCLUSION
In conclusion, it was found that it is possible to measure reliable interactions between a core particle and a shell using...
liquid-cell electron microscopy. We found that the interactions between a titania core and silica shell could be tuned over a large range of ionic strengths. The interactions of a sphere within a shell were found to be significantly more long-ranged compared to the interactions between two spheres under the same conditions. It was also observed that the core particle could approach the shell more closely when no salt was added, compared to the case for moderate salt concentrations (0.5 and 1 mM). Finite-element calculations confirmed this to be due to a flat electric potential within the rattle geometry in deionized water. Furthermore, for salt concentrations above 50 mM, the core particle spent more time close to the shell wall than in the middle of the rattle geometry. Simulations confirmed that hydrodynamic slowing down of the core particle plays a significant role, while calculations also showed a secondary minimum in the potential of a few kBT was probable at such high salt concentrations, as well, contributing to the above-mentioned behavior. Due to the limit of our 2D projected experimental data, the extent of both effects could not be determined accurately experimentally.

Lastly, the interactions between a gold nanosphere and a silica nanoshell were measured in aqueous solutions. We found that, due to the flat electric potential within the shell, the nanosphere is less stable within the shell in deionized water, compared to when a moderate amount of salt was added (0.5–5 mM). The results indicate that liquid-cell electron microscopy is a powerful tool to measure interactions of nanoparticles in water, where a high spatial resolution is a requirement.

METHODS

Liquid-Cell STEM. In order to image the rattle-type particles in the electron microscope, we used a liquid-flow TEM holder with corresponding microchips (Hummingbird Scientific, USA). The microchips support 50 nm thick amorphous silicon nitride (SiN) windows with lateral dimensions of 50 by 200 μm². A sample cell consists of two chips separated by a spacer of 250 or 1000 nm in height, depending on the size of the rattles. The two Si chips were glow-discharged for 1 min prior to the experiment in order to make their surfaces more hydrophilic. The microchip with spacer was then placed in a dedicated holder. A 1 μL droplet of the dispersion of rattle-type particles in deionized water was drop-cast onto the microchip. The second microchip was placed on the bottom chip with the hydrophilic side facing the opposite chip. The excess liquid was removed with filter paper.

The liquid-cell STEM experiments were carried out using a transmission electron microscope (Tecnai-F20, Thermo-Fischer Scientific), equipped with a field emission gun, and operating at 200 kV. The semi-convergence angle of the electron probe was 10 mrad. The ADF detector was used with a camera length of 120 mm. Image series were acquired with TEM imaging and analysis software (TIA). For the experiments with titania@water@silica rattle-type particles, the beam current measured via the fluorescent screen in vacuum was 37 pA for all videos unless specified differently. A frame recording time of 1 s was used. The number of pixels was 512 × 512, which resulted in a pixel size of 4.4–8.8 nm depending on the magnification. These settings resulted in an electron dose rate of 12–45 e⁻ nm⁻² s⁻¹. For the experiments with gold@water@silica nanorattles, the beam current in vacuum was 85 pA. A frame time of 1 s was used. The number of pixels was 512 × 512 pixels, which resulted in a pixel size of 3.14 nm. This corresponded to an electron dose rate of 206 e⁻ nm⁻² s⁻¹. The image series acquisitions were at least 180 frames long.

After the holder was inserted into the microscope and before image acquisition started, deionized water was flowed through the cell at a rate of 2 μL/min for 45 min. At least three rattle-type particles in different parts of the liquid cell were then imaged while the flow was turned off. We did not observe any influence of the flow on the particle mobility within the shell but were concerned about mechanical vibrations and thus left the flow off during measurements. The shell of the rattle-type particle was stuck to the top chip of the liquid cell, and therefore, only the core particle inside could move. Each particle was imaged separately and for 180–600 s per LiCl concentration. After image series acquisition for one LiCl concentration was completed, the next, more highly concentrated LiCl solution was flowed into the liquid cell at a rate of 2 μL/min for at least 10 min. The flow was then turned off again for image series acquisition. This was repeated for all different salt concentrations for the same three particles. At the end of the experiment, a solution of pH 2 (10.0 mM HCl) was flowed into the cell. This made the silica shell charge-neutral and the core particle irreversibly attached to the shell (Figure S10). This allowed us to measure the size of the core particle for that particular rattle-type particle.

Image Processing. The procedure is shown in Figure 2 of the main text. We used ImageJ (1.51a) and Mathematica (Wolfram, v12.2) to analyze the recordings. We used ImageJ to binarize the individual frames of the videos. These binarized images were then used as a mask to remove the background of the original images. This leaves us with the original intensity of the pixels carrying signal of the presence of the particle, while all other pixels are made black. We then averaged all those frames into a single image. This average image was then deconvoluted with an image of a titania particle with radius Rcore = 170 nm, as calculated with CASINO (version 3.3.0.4; see the section on simulating static ADF-STEM images). For this, we used a Richardson–Lucy deconvolution algorithm in Mathematica. The remaining image gave a map of the probability of finding the center of the core particle in a certain projected part of the shell, which was corrected for the volume in the plane perpendicular to the image, as explained in the Supporting Information.

Reconstructing the 3D Interaction Potential. Our experimental LC-STEM image series are 2D projections of a 3D system. In order to compare the experimental data to calculations, we need to reconstruct the effect of a 3D interaction potential between the core particle and the shell caused by the 2D projection. As the core particle is moving around randomly via Brownian motion, the probability P(r) can be translated to a interaction potential U(r) via

\[
U(r) = -kT \ln(P(r))
\]

(3)

Here, \( r \) is the radial spherical coordinate. However, since the probability from our experiments is a 3D probability projected on a 2D plane, a 3D potential needs to be projected on a 2D plane, while correcting for the spherical geometry in the third dimension (Supporting Information). We do this by translating a trial potential

\[
U_{\text{trial}} = A e^{-\kappa r} / r
\]

(4)

into a projected probability. Here, \( \kappa \) and \( A \) are fit parameters. The fit parameters for which the projected probability distribution matches the experimental data most accurately are assumed to be the parameters in the 3D interaction potential in our experiments.

To translate the trial potential to a projected probability, we make a list of available \( z_i \) coordinates per cylindrical coordinate \( \rho_i \), where the maximum \( z \) coordinate at projected radial coordinate \( \rho \) is given by

\[
z_{\text{max}} = \sqrt{(R_{\text{shell}} - R_{\text{core}})^2 - \rho^2}
\]

(5)

Then we make a list of all the available 3D radial coordinates \( r \) within the cylindrical coordinate \( \rho_i \):

\[
r = \sqrt{\rho_i^2 + z_i^2}
\]

(6)

The projected probability \( P(\rho) \) is then calculated by averaging all 3D probabilities \( P(\rho) \) that fall into the projected radial coordinates \( \rho \) via

\[
P(\rho) = \langle P(z_{1,2,\ldots}) \rangle = \langle e^{-U(z_{1,2,\ldots})/kT} \rangle
\]

(7)
In the final result, the interaction potential is expressed as a function of the core–shell separation distance \( d = (R_{\text{shell}} - R_{\text{core}}) - r \).

**Interaction Potential Calculations.** Electrostatic Interaction.

We performed finite element calculations using COMSOL Multiphysics (VS.5). The rattle geometry was used in an axisymmetric calculation. We solved the nonlinear Poisson–Boltzmann equation for a symmetric 1:1 electrolyte:

\[
-\varepsilon_0 \nabla^2 \psi = \frac{2 \varepsilon_0 \sinh \left( \frac{\varepsilon \psi}{k_B T} \right)}{k_B T}
\]  

(8)

Here, \( \psi \) is the electric potential, \( \varepsilon_0 \) is the permittivity of vacuum, \( \varepsilon \) is the dielectric constant of the liquid, \( \varepsilon_0 \) is the monovalent salt concentration, \( \varepsilon \) is the electron charge, \( k_B \) is the Boltzmann constant, and \( T \) is the temperature. On the surface of the core and the shell, we put constant surface potential boundary conditions.

We exploited the rotational symmetry of the system to minimize the number of elements required. Due to the large slopes in ion concentration near the charged surfaces, a fine mapped mesh was applied from the boundary of the charged surface to a distance of one distance from the center of the shell.

**van der Waals Interaction.** To calculate the vdW interaction between a sphere and a shell, a relationship is required to determine the interaction between a sphere and an element located at a point a distance \( d \) away from the sphere surface.80 By integrating over the shell volume, we obtain the vdW interaction between a sphere and a shell at a distance \( d \) from the shell wall.

\[
U_{vdW}(d) = \frac{-16\pi \varepsilon \sigma^3}{3} \int_0^\infty \int_{R_{\text{core}} + d(\theta, \phi)}^{R_{\text{shell}} + d(\theta, \phi)} r^2 \sin(\theta) d\theta d\phi \left( \frac{1}{r^2} - \frac{1}{R_{\text{core}}^2} \right)^3
\]  

(12)

Here, \( \Lambda \) is the Hamaker constant, \( T_{\text{shell}} \) is the thickness of the shell, and \( r \) and \( \theta \) are the radial and polar angles in a spherical coordinate system, respectively. Finally, \( d(\theta, \phi) \) is the distance of the core to different parts of the shell depending on the polar angle \( \theta \) and the displacement from the center of the shell:

\[
d(\theta, \phi) = \sqrt{(R_{\text{shell}} - R_{\text{core}})^2 + a^2 \sin^2(\theta)^2 - a \cos(\theta)}
\]  

(13)

Here, \( R_{\text{shell}} \) and \( R_{\text{core}} \) are the radius of the core and the inner radius of the shell, respectively. For the titania@water@silica particles, the used Hamaker constant was \( A_{123} = 6.9 \times 10^{-21} \) J calculated via the full Lifshitz theory.81 The used shell thickness was 25 nm. Equation 12 was integrated numerically in Mathematica.

**Simulating Static ADF-STEM Images.** To understand the influence of hydrodynamics and the errors in the measurements, we simulated ADF-STEM images of a moving particle within a shell. Therefore, we are first required to simulate ADF-STEM images for a static particle. For this purpose, we simulated ADF-STEM images using the CASINO software (version 3.3.0.4).82–84 The physics model used for the total and partial cross sections in the simulation software was that of an empirical analytical fit to the Mott cross sections by Browning et al.85 The specific parameters of the sample and the electron probe were taken to be as close to the experimental parameters as possible. However, we chose to use 256 by 256 pixels and twice the pixel size as in the experiments (which had 512 by 512 pixels) in order to reduce the computation time.

We put a 340 nm titania particle at different positions within a shell with a 700 nm inner diameter within a water layer of a micrometer. The electron probe was set to have a semiconvergence angle of 10 mrad and a diameter of 1 nm. The beam distribution was Gaussian. The electron probe had an energy of 200 keV and had its focal point on the middle of the rattle particle geometry. The top of the shell of the rattle geometry was at the same height as the top of the water layer. The pixel size was 8.9 nm, and the number of simulated electrons per pixel \( N \) was 3528, as calculated from the beam current \( I = 0.357 \) nA and the pixel dwell time \( t = 1/256^2 \) s via

\[
N = \frac{I}{te}
\]  

(14)

where \( e \) is the electron charge. The ADF detector with a quantum efficiency of 100% was set to have a minimum and maximum semiangle of 15 and 300 mrad, respectively. In total, 41 static images of a particle in different positions in the shell were simulated.

**Simulating ADF-STEM Images of a Diffusing Particle in a Shell.** We first calculated the diffusion coefficient of the particle in the shell. The diffusion coefficient of the particle depended on the position within the shell, as well as the direction of the displacement. The mobility of the core particle toward the shell (radial diffusion) and along the shell wall (perpendicular diffusion) was investigated using finite-element calculations. More details can be found in the Supporting Information.

When the directional diffusion coefficients at all positions of the core within the shell were known, the particle motion could be simulated. For every pixel that was scanned, the particle was moved in a random direction with a velocity in the perpendicular and radial direction that was dependent on its current position within the shell. The random direction of the perpendicular vector \( \mathbf{n}_y \) was coded by creating two normalized vectors, \( \mathbf{v}_x \) and \( \mathbf{v}_y \), that were perpendicular to the radial direction and choosing a random real number \( n_i \) between 0 and 2\( \pi \). The direction of the perpendicular vector was then chosen using this random real number \( n_i \) via

\[
\mathbf{n}_y = n_1 \cos(n_i) + n_2 \sin(n_i)
\]  

(15)

Now that the direction of the radial displacement and the perpendicular displacement is decided, we let the particle move a random step, within the pixel dwell time \( \Delta t_i \) in the radial and perpendicular directions based on a normal distribution with standard deviations \( \sigma_r \) and \( \sigma_p \), respectively. These are related to the radial and perpendicular diffusion coefficients, \( D_r \) and \( D_p \), at the current position via

\[
\sigma_r(r) = \sqrt{2D_r(r)\Delta t_i}
\]  

(16)

\[
\sigma_p(r) = \sqrt{4D_p(r)\Delta t_i}
\]  

(17)

The particle was free to move up until a sharp barrier a certain distance away from the shell wall. When the new simulated position of the particle was not allowed by the imposed barrier, a new position of the particle was calculated from the old position until that new position was allowed.

When the position of the particle was known for every pixel scanned, the image of the moving particle was formed. This was achieved by taking the position of the particle at the time and finding the three static ADF-STEM images that included the core particle closest to that position. The pixel was then given an intensity based on the weighted mean of that same pixel in the three chosen ADF-STEM...
images. The mean was weighted linearly by the absolute distance of the particle position in the static image compared to the real position. This was done for every pixel in an image and for at least 180 images.

ASSOCIATED CONTENT
- Supporting Information: The Supporting Information is available free of charge at https://pubs.acs.org/doi/10.1021/acsnano.1c03140.
  - Movie S1: Concatenated individual videos of a titania@water@silica rattle-type particle in pure water at different electron dose rates; electron dose rates shown in video in units of e⁻⁻ nm⁻² s⁻¹ (AVI)
  - Movie S2: Concatenated individual videos of a titania@water@silica rattle-type particle in 10.0 mM LiCl at different electron dose rates; electron dose rates shown in video in units of e⁻⁻ nm⁻² s⁻¹ (AVI)
  - Movie S3: Concatenated individual videos of a titania@water@silica rattle-type particle at different pH; electron dose rate was 95 e⁻⁻ nm⁻² s⁻¹ (AVI)
  - Movie S4: Concatenated individual videos of gold@water@silica rattle-type particles at different pH; electron dose rate was 179 e⁻⁻ nm⁻² s⁻¹ (AVI)
  - Movie S5: Concatenated individual videos of a gold@water@silica rattle-type particle in 1.00 mM LiCl at different electron dose rates; electron dose rates shown in video in units of e⁻⁻ nm⁻² s⁻¹ (AVI)
  - Movie S6: Concatenated individual videos of a titania@water@silica rattle-type particle at various salt concentrations; electron dose rate was 45 e⁻⁻ nm⁻² s⁻¹ (AVI)
  - Movie S7: Concatenated individual videos of a gold@water@silica rattle-type particle at various salt concentrations; electron dose rate was 206 e⁻⁻ nm⁻² s⁻¹ (AVI)
  - Movie S8: Four gold@water@silica nanorattles. The top two gold particles are mobile; however, the particle in the middle is attached to the shell and only gets loose due to interactions with the electron beam. The bottom gold particle is mobile, but the electron beam is causing it to sometimes stick to the shell wall for a frame. This shows that gold@void@silica nanorattles may sometimes be unstable in pure water due to a flat electric potential within the shell geometry; electron dose rate was 206 e⁻⁻ nm⁻² s⁻¹ (AVI)
  - Synthesis details; zeta-potential measurements; volume corrections for the projected data; additional details and checks on the calculations on electrostatic; van der Waals, and hydrodynamic interactions; influence of the electron beam; estimation of the resolution (PDF)

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Complete contact information is available at: https://pubs.acs.org/doi/10.1021/acsnano.1c03140

Author Contributions
T.A.J.W. performed the LC-STEM experiments, data analysis, the calculations, and the simulations and wrote the manuscript. K.W. synthesized the rattle particles under supervision of D.N. A.G.C. helped with useful tips regarding the experimental data analysis. J.d.G. helped set up the finite-element calculations and provided helpful advice on the theoretical side of the project. A.I. helped with the concept of flat potentials within the rattles. M.A.v.H. obtained the funding for the project and supervised the project. A.v.B. supervised the project and co-wrote the manuscript. All authors have given approval for the final version of the manuscript.

Notes
This manuscript was previously uploaded to a preprint server: 10.26434/chemrxiv.14459826.v1. The authors declare no competing financial interest.

ACKNOWLEDGMENTS
We acknowledge Wessel Vlug for his early work on interactions within rattle-type particles. This project has received funding from the European Research Council (ERC) via the ERC Consolidator Grant NANO-INSITU (Grant No. 683076). K.W. and D.N. acknowledge the support from the Ministry of Education, Culture, Sports, Science and Technology, Japan (Materials Processing Science project (‘Materrealize’) of MEXT, Grant No. JPMXP019192801). J.d.G. thanks NWO for funding through Start-Up Grant No. 740.018.013 and through association with the EU-FET Project No. NANOPHLOW (766972) within Horizon 2020.

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