The effect of a scanning flat fold mirror on a cosmic microwave background B-mode experiment
William F. Grainger, Chris E. North, and Peter. A. R. Ade

Citation: Review of Scientific Instruments 82, 064502 (2011); doi: 10.1063/1.3598342
View online: http://dx.doi.org/10.1063/1.3598342
View Table of Contents: http://scitation.aip.org/content/aip/journal/rsi/82/6?ver=pdfcov
Published by the AIP Publishing

Articles you may be interested in
Publisher's Note: “Modulation of cosmic microwave background polarization with a warm rapidly rotating half-wave plate on the Atacama B-Mode Search instrument” [Rev. Sci. Instrum. 85, 024501 (2014)]
Rev. Sci. Instrum. 85, 039901 (2014); 10.1063/1.4867655

Modulation of cosmic microwave background polarization with a warm rapidly rotating half-wave plate on the Atacama B-Mode Search instrument
Rev. Sci. Instrum. 85, 024501 (2014); 10.1063/1.4862058

Note: Innovative demodulation scheme for coherent detectors in cosmic microwave background experiments
Rev. Sci. Instrum. 83, 056104 (2012); 10.1063/1.4719922

Polarization of the Cosmic Microwave Background from non-uniform reionization
AIP Conf. Proc. 609, 271 (2002); 10.1063/1.1471860

The Milano polarization experiment devoted to the study of the cosmic microwave background
AIP Conf. Proc. 609, 164 (2002); 10.1063/1.1471841
The effect of a scanning flat fold mirror on a cosmic microwave background B-mode experiment

William F. Grainger, Chris E. North, and Peter. A. R. Ade
Astronomy Instrumentation Group, Cardiff School of Physics and Astronomy, Cardiff University, Queens Buildings, The Parade, Cardiff CF24 3AA, United Kingdom

(Received 1 April 2011; accepted 17 May 2011; published online 29 June 2011)

We investigate the possibility of using a flat-fold beam steering mirror for a cosmic microwave background B-mode experiment. An aluminium flat-fold mirror is found to add \( \sim 0.075\% \) polarization, which varies in a scan synchronous way. Time-domain simulations of a realistic scanning pattern are performed, and the effect on the power-spectrum illustrated, and a possible method of correction applied. © 2011 American Institute of Physics. [doi:10.1063/1.3598342]

I. INTRODUCTION

The prevailing \( \Lambda \)CDM cosmological model has been very successful in explaining many observations of the universe. However, inflation – exponential expansion within the first \( \sim 10^{-35} \) s – has many uncertain details; indeed it lacks strong confirmation. Inflationary models predict a background of gravity waves\(^{1,9,18,20,21}\) which produce a curl-like, or “B-mode” pattern of polarization on the cosmic microwave background (CMB) on scales greater than 1°, which cannot be produced by density perturbations.\(^{11,23}\) The amplitude of this signal is characterized by the tensor-to-scalar ratio, \( r \), which is constrained by current measurements of the temperature power spectrum and temperature-polarization cross-correlation to a value \( r < 0.20.\(^{12}\) To put tight constraints on inflationary models\(^3\) we need to detect the primordial B-mode signal, or constrain it for \( r < 0.01.\) This requires measurement of polarization fluctuations at the level of 10 nK.

To measure this signal level is challenging, and good control of systematics is required.\(^{10}\) A number of ground-based (QUIET,\(^{19}\) PolarBear\(^\dagger\)), balloon-based (EBEX,\(^7\) Spider\(^4\)), and satellite-based (Planck\(^{14,17}\)) experiments have been, or are close to being, fielded with the raw sensitivity to detect the B-mode signal if it is present at a reasonable level. These experiments are all designed to have low, and stable, instrumental polarization, and often include a modulation strategy to assist with reducing systematics and mitigating against 1/f noise. The majority of these experiments hold their optics stationary with respect to the receiver, and scan the cryostat and optics together; a notable exception being the Tenerife experiment.\(^5\) Scanning the cryostat places requirements on the stability with respect to accelerations and tilts. Although cryogenic receivers have been demonstrated that are stable at different tilt angles,\(^8\) the sensitivity to accelerations has not been demonstrated. A system can be imagined, however, which combines a stationary receiver with a fold mirror. Besides the simplification of the cryogenic requirements, the large reduction in the mass of moving components would make the design of the steerable mount much simpler.

We investigate such a system in this paper. In Sec. II we describe the system, and review the production of polarization from reflections. In Sec. III we describe a fiducial scan strategy and simulation pipeline. Results from this pipeline are then presented and discussed, along with other potential problems in Sec. IV.

II. METHOD

For this investigation, we consider a horn fed receiver and compact range antenna (CRA), placed in a groundscreen, nominally observing the horizon. The output beam of the CRA is then steered to the sky with a single, flat, fold mirror. Although the flat mirror would be large; \( \sim 4 \times 4m\), such a system can be considered. The flat mirror is then tipped and tilted such that the beam of the telescope moves across the sky to allow observations.

Off-normal reflections, as caused by this folding, induce a polarization. The effect is well known and is the principle behind, for example, the “pile-of-plates polarizer.” The Fresnel equations give the reflection coefficients for incident angle \( \theta_i \) and transmission angle \( \theta_t \) for an incident wave with E-field parallel to the boundary, \( R_\parallel \) and \( R_\perp \),

\[
R_\parallel = \left( \frac{\tan^2(\theta_t - \theta_i)}{\tan^2(\theta_t + \theta_i)} \right), \tag{1}
\]

\[
R_\perp = \left( \frac{\sin^2(\theta_t - \theta_i)}{\sin^2(\theta_t + \theta_i)} \right). \tag{2}
\]

For a metal plate, we use the relation for the complex index of refraction,

\[
(n + i\kappa)^2 = \epsilon' + i\epsilon''. \tag{3}
\]

For a general dielectric, the conductivity \( \sigma \) is given by \( \sigma = \omega\epsilon''\epsilon_0 \) where \( \omega = 2\pi f \) and \( f \) is the radiation frequency. For a good conductor, we can assume \( \epsilon' \ll \epsilon'' \), and so

\[
n^2 = \frac{\sigma}{2\omega\epsilon_0}. \tag{4}
\]

Plugging this into Snell’s law allows calculation of \( R_\parallel \) and \( R_\perp \). For a pure aluminium plate, \( 1/\sigma = \rho = 28.2 \times 10^{-9} \Omega m \), we find \( R_\parallel = 0.9970 \) and \( R_\perp = 0.9985 \). Thus an unpolarized input reflected with \( \theta_t = 45^\circ \) would have an overall polarization of 0.075% This ignores the phase-delay from the reflections, which elliptically polarizes the reflected beam, producing both circular polarization and rotating the plane of
polarization. Using a Drude-Lorentz model to calculate $n$ and $\kappa$ for aluminium at 90 GHz,\cite{24} we calculate that the plane of polarization is rotated by an additional $\sim 10^{-9}$ degrees when the phase delay is included. Ignoring this is then valid as this is a much smaller than the effect from differential reflection ($\sim 0.2^\circ$). The reflection is a total power to polarization conversion ($T \rightarrow Q, U$); in the context of a CMB polarization measurement the total power is 2.7 K, and so the induced polarized signal is then $\sim 200 \mu$K, higher than even the EE polarization spectrum. However, the signal is changing consistently with the scan, and so is varying on different scales from the CMB signals of interest and so could, in principle, be removed. In Sec. III, we describe the pipeline with which we investigate the effect on CMB reconstruction and $C_\ell$ estimation.

We note in passing that it is possible to construct a two mirror system that provides a fold with no net polarization. Consider a beam travelling along the $x$ axis. The first mirror, mounted at 45° to the $yz$ plane, then reflects the beam so it is travelling along the $y$ axis, and the second, mounted at 45° to the $xy$ plane, reflects that beam along the $z$. As the reflection axes have switched, both input $E_x$ and $E_y$ receive an attenuating factor of $R_x R_y$. Any net polarization is then due to differences between the conductivity of the mirrors. If the two mirrors are fixed relative to each other, and allowed to rotate about the $x$ axis, the beam can be steered. A second set of mirrors, in a similar configuration, can be added to allow full beam steering around the sky. This is illustrated in Fig. 1.

III. SCAN STRATEGY AND PIPELINE

We simulate observations with the following four step pipeline. First, time ordered data (TOD) is simulated with 100 Hz sampling for four 3-h observation periods, corresponding to a day of observations, and the sky location (RA, Dec), telescope pointing direction (az, el), and observed $E_1^2$ and $E_2^2$ recorded. The input CMB maps were produced by simulating a power spectrum with CAMB,\cite{16} and producing a realization with the HEALPIX (Refs. 6 and 18) synfast routine. This input all-sky map was also convolved with a Gaussian beam with FWHM of 5.5 arc min. Parameters used in the simulation are listed in Table I. Note that we include the monopole in this simulation, with a temperature of 2.7 K and so $E_x^2 \sim E_y^2 \sim 1.3$ K.

It is generally desirable for ground-based and suborbital experiments to scan the sky at constant elevation to minimize the effect of variable airmass. We follow this and consider the proposed Clover scan strategy, the optimization of which is fully described elsewhere.\cite{18} The strategy is to perform azimuthal scans at fixed elevation (nominally 45°) as the chosen sky patch rises for around 1 h, continually adjusting the azimuthal center to achieve as circular a patch as possible. Once the patch has risen sufficiently through the scan, the elevation is increased, nominally to $\sim 60^\circ$, and the patch continues to rise for another 3 h. The same strategy is used as the patch sets, giving four distinct data streams for a single patch during a 8-12 h observation period.

The second step in the pipeline is to take the pointing from the TOD data, determine the angle of the flat folding mirror, rotate the observed $E_1^2$ and $E_2^2$ to align with the plane of the mirror, apply the calculated $R_x$ and $R_y$, and then rotate back. The TOD is then naively binned to produce T, Q, and U maps, following the map-making scheme outlined in Ref. 3, and then written out as a HEALPIX format FITS files. We make maps at $N_{side} = 512$ so that the multipole range $\ell \sim 100$ to 1000 is retrievable, and avoid holes in the maps by simulating a five pixel focal plane. The pixel angular positions from boresight are listed in Table I.

Finally, the angular power spectrum (APS) coefficients $C_\ell$ are estimated using the anafast HEALPIX routine. We apply a circular mask of radius 10° with a simple cosine-squared taper of width 2° at the edge.

A. Determination of angles

In order to determine the effect for a mirror at an arbitrary orientation, two angles are required; the angle of incidence, $\theta_i$ and the angle, $\beta$, between the mirror and the horizon as seen by the incident photons. Consider the flat fold mirror to be at the origin, and the unit vector a points to the dewar, and b points to the position on the sky being observed. This is illustrated in Fig. 2. $\alpha$ is the angle between a and b. In polar coordinates, $a = (1, 90^\circ, 180^\circ)$ and $b = (1, \theta_s, \phi)$ where $90 - \theta_s$ and $\phi$ are the elevation and azimuth of the sky location. Converting into Cartesian coordinates, we have $a = (-1, 0, 0)$ and $b = (\cos \phi, \sin \phi, 0)$.

\begin{table}[h]
\centering
\caption{Simulation parameters. Detector positions are given in (az, el) in the telescope frame.}
\begin{tabular}{ll}

\hline
Parameter & Value \\
\hline
Telescope location & Atacama desert \\
Patch centre & 9 h 00 m, –44°40’0’’ \\
Patch radius & 10° \\
Azimuthal scan speed & 0.5 deg/s \\
Nominal elevations & 45, 60 deg \\
Observing frequency & 90 GHz \\
Data rate & 100 Hz \\
Resitivity of aluminium & $28.2 \times 10^{-9}$ $\Omega$m \\
Input $x$ & 0.1 \\
Detector 1 position & (0.0) arc min \\
Detector 2 position & (14.8, 14.8) arc min \\
Detector 3 position & (29.6, 29.6) arc min \\
Detector 4 position & (36.9, 7.4) arc min \\
Detector 5 position & (51.7, 22.1) arc min \\
\hline
\end{tabular}
\end{table}
and \( \mathbf{b} = (\sin \theta_e \cos \phi, \sin \theta_e \sin \phi, \cos \theta_e) \). To determine \( \alpha \), we take the dot-product of \( \mathbf{a} \) and \( \mathbf{b} \) and get

\[
\mathbf{a} \cdot \mathbf{b} = \cos \alpha = -\sin \theta_e \cos \phi. \tag{5}
\]

As the angles of incidence and reflection, \( \theta_i \) and \( \theta_r \) are equal, we have

\[
\theta_i = 1/2\alpha = 1/2 \arccos(- \sin \theta_e \cos \phi). \tag{6}
\]

We define \( E_x \) to be parallel to the horizon, and \( E_y \) to be “upwards” towards the zenith. We require the angle \( \beta \) by which \( E_x \) and \( E_y \) need to be rotated (around the line of sight) so that the rotated \( E_x \) is parallel to the mirror. We define \( \mathbf{c} \), a unit vector that points in the same direction as \( E_x \), so, in polar coordinates, \( c = (1, 90^\circ, \phi + 90^\circ) \). \( \mathbf{a} \wedge \mathbf{b} \) is parallel to the mirror. By taking the dot product of \( \mathbf{a} \wedge \mathbf{b} \) with \( \mathbf{c} \), we can determine the angle \( \beta \) as

\[
(\mathbf{a} \wedge \mathbf{b}) \cdot \mathbf{c} = |(\mathbf{a} \wedge \mathbf{b})||\mathbf{c}| \cos \beta. \tag{7}
\]

After some algebra,

\[
r = \arccos(\cos^2 \phi). \tag{8}
\]

Thus we have the angle of incidence, \( \theta_e \), required for the calculation above, and we have the angle, \( \beta \), so that the \( R_\parallel \) and \( R_\perp \) factors can be applied to the rotated \( E_x \) and \( E_y \).

### IV. RESULTS AND DISCUSSION

#### A. Simulation results

We use CAMB to simulate a sky, observe it with our scanning strategy code, and follow the pipeline through to calculate power spectra. First we test our pipeline by ignoring the effect of the fold mirror; resultant APS are shown in Fig. 3. In the region of interest (\( \ell \sim 100-1000 \)) the output spectra match the input spectra well for TT and EE. The spectra from the masked pipeline maps for TT and EE are slightly suppressed for larger \( \ell \); 5% at \( \ell \sim 900 \) when compared to the spectra made from the full sky maps. However, as the spectra from the masked full sky maps are also suppressed, we conclude that this is due to the effect of the partial sky mask and fairly naive apodization procedure. Similarly, the BB spectra from the masked map is higher than the all-sky map, but as the pipeline BB spectra agrees with the masked all-sky map BB spectra, we conclude that it is the mask rather than the map-making procedure which is increasing the BB power. Although this level of analysis is not sufficient for a full B-mode experiment, this level of analysis is sufficient for investigating the effect of the flat-fold mirror.

We then apply the effect of a flat fold mirror in the pipeline, using the resistivity of aluminium of \( 28.2 \times 10^{-3} \) \( \Omega \)m, and observations at 90 GHz. A section of the time stream is shown in Fig. 4, both the input and output \( E_x^2 \) and the azimuth of the observed sky location. The correlation between induced polarization with observed sky azimuth is clear.

The induced polarization is big, and so it is reasonable to remove it without requiring the entire data set. By applying the reverse of the observing algorithm, we can determine a “pre-mirror” \( E_x \) and \( E_y \) for a given mirror resistivity. We use \( \Sigma(E_x^2 - E_y^2) \), summed over the day of observation for a particular pixel, as a measure of the amount of polarization, and minimize it by varying the resistivity, using the Nelder-Mead simplex direct search,\(^1\) implemented in MATLAB. This time-line can then be re-inserted into the pipeline, maps made and spectra computed. The resultant APS are shown in Fig. 3. We see that in the range \( \ell \sim 100-1000 \), the TT, EE, and BB spectra all match the pipeline output as before. In order to show problems more clearly, we also plot the difference between the spectra produced from the maps with and without the fold mirror. These are shown against \( \ell \) in Fig. 5. We find that the TT and EE spectra are reconstructed well, with less than 1% difference between \( \ell \) of 250 and 900. The BB spectra shows both fluctuation of \( \sim 1\% \) and an overall offset of 2.5% over the same \( \ell \) range.

#### B. Noise

The shortest required observing time, for a generalized CMB experiment, would be achieved using a photon noise limited telescope at a good site. For a instrument such as Clover, situated in the Atacama desert, the system NET is

---

FIG. 2. Fiducial geometry considered for calculating the relevant angles. Top left: the telescope beam from the dewar (direction a) to the sky (b), directed at the azimuthal polar coordinates (\( \theta_e, \phi \)). Bottom left: the angle \( \alpha \) through which the beam is reflected by the mirror. Right: \( E_x \) and \( E_y \), the two polarization vectors on the sky.
FIG. 3. TT, EE, and BB spectra from various maps. Dashed-dotted-dotted-dotted line is the input spectra, as simulated by CAMB. Dotted line is the all sky map, masked with the same mask used for the observed patches. Solid is after our pipeline, but with no mirror. Dashed is the spectra after having been observed with a flat fold mirror. Dotted-dashed is the spectra after observed, but with the fitting algorithm (described in the text) applied.

175 μK √s. With a 100 Hz data stream, this noise level overwhelms the induced polarization signal from T → Q,U mixing. However, simple binning by a factor of ten is sufficient to see the induced polarization signal in the presence of white noise. If we add white noise at the level of 175 μK √s, with an ρ = 28.2 × 10⁻⁹ Ωm, the best fitting resistivity returned with this procedure is 28.8 × 10⁻⁹ Ωm.

Detector 1/f noise is assumed to be unimportant, assuming a detector-based modulation strategy is implemented (e.g., using a rotating or stepped half-wave plate such as EBEX, or a fast detector switching such as QUIET). Atmospheric 1/f total power variations contributes strongly however as the effect of the reflection is a total power to polarization conversion. Thus the atmospheric 1/f becomes a polarization 1/f term which does not get removed by any modulation strategy. A straightforward differencing strategy, for example differencing successive samples during azimuthal scanning, or differencing two adjacent detectors, to remove this varying atmospheric contribution is likely to be the most efficient method, but would reduce the effective observing time by a factor of two.

C. Temperature variations

The resistivity of aluminium varies with temperature, and so the induced polarization will vary with temperature. Given
FIG. 4. Upper plot: time stream of the input and observed $E_x$ for a noiseless simulation, with a $28.2 \times 10^{-9} \Omega \text{m}$ fold mirror. Lower plot: time stream of the telescope azimuth.

a resistivity at room temperature of $\rho_0 = 28.2 \times 10^{-9} \Omega \text{m}$, the difference between the two polarization reflection coefficients is 0.075%. We introduce a temperature coefficient of resistance, $\rho_T$, of $3.8 \times 10^{-3} \text{K}^{-1}$, with $\rho = \rho_0 (1 + \rho_T \Delta T)$. Varying the temperature by 20 °C gives a difference of 0.078% between the two polarization reflection coefficients, meaning that the $T \rightarrow Q,U$ mixing varies by $\sim 7\%$. For a reasonably large flat fold mirror – in this case the flat is $\sim 2\text{m}$ diameter – the temperature variation is likely to be on the time scale of hours, driven largely by the ambient temperature variations. Such variations should be removable by fitting the resistivity to the data over different time scales on a pixel-by-pixel basis. We note that, apart from the pixel on the optical axis, each pixel will see a section of the mirror whose location varies in a predictable way with azimuth (and elevation) and so fitting with respect to mirror position might also be required. In this case, the error on the fit can be reduced by fitting multiple pixel data simultaneously to produce a mirror resistivity map.

D. Oxide growth

The polarizing effect of the fold mirror comes from its resistivity. As such, effects that alter the resistivity alter the polarizing effect. Aluminium grows an oxide layer very quickly, which then hydrates. The hydrated aluminium oxide can then be degraded chemically, or by physical damage to the surface. Such a surface is thin (5-15 nm) and so does not change the resistivity by a large amount. It is not unreasonable to assume that there will be changes to the surface during an extended observing campaign, both with oxide thickness and additional surface contamination. As with the temperature variation, contamination would almost certainly be localised, and so fitting resistivity with respect to mirror position would probably be required. However such changes would be expected to be slow (time scales of days or more), or at least sudden and stable, and so more data is available to fit out the effect. As a result, we expect the resistivity variation from surface oxidation and contamination to be better characterised than the temperature variation.

E. Polarized foregrounds

The work so far has assumed that the light incident on the flat-fold mirror is polarized at a very low level, and that the majority of the polarized signal comes from the flat-fold mirror. This is the case when considering the CMB only, where the polarization signal has zero mean. These assumptions do not hold, however, when observing an arbitrary patch of sky, where both synchrotron and dust from the galaxy is expected to be polarized at the $\sim 1 - 10\%$ level, with a total intensity of $10 - 100 \mu K$ close to the galactic plane, but down to $\lesssim 1 \mu K$ at...
high galactic latitudes. As such, we would recommend this method only be used in regions of known low foreground emission, where the resulting error in polarization reconstruction would be small. Over sufficiently large areas of sky the magnitude of the effect could be modelled, and in regions with relatively little large-scale variation in the foreground emission would be small. Over sufficiently large areas of sky the effect could be a constant offset, similar to an additional absolute calibration error. The areas of sky observed by most B-mode experiments are selected to meet these requirements.

In order to test this, we re-ran the simulation with some fiducial dust and synchrotron models added. After applying the same method as discussed above, the map-plane residuals are large; we see residuals of ±20 to −40 µK in the Q map, in comparison with the signal level of ±20 µK across the map. We leave fully developing this method to work in the presence of significant polarized foregrounds for future work.

V. CONCLUSIONS

We have analyzed the effect of a flat-fold mirror on polarization measurements of the CMB. In the case of no foregrounds and no noise with no corrections, we find that the E and B spectra are heavily contaminated by the mixing of total power to polarization signal. However, as the CMB is expected to have a net polarization of zero, the effect can be fitted out. In the case of having a net polarization, such as in a real observation of the sky, the reconstructed maps contain significant residuals.

ACKNOWLEDGMENTS

We thank Enzo Pascale and Giorgio Savini for useful discussions during this work. Some of the results in this paper have been derived using the HEALPIX.6

1L. F. Abbott and M. B. Wise, Nucl. Phys. 244, 541 (1984).
2J. Bock, S. Church, M. Devlin, G. Hinshaw, A. Lange, A. Lee, L. Page, B. Partridge, J. Ruhl, M. Tegmark, P. Timbie, R. Weiss, B. Winston, and M. Zaldarriaga, e-print arXiv:astro-ph/0604101v1.
3M. L. Brown, A. Challinor, C. E. North, B. R. Johnson, D. O’Dea, and D. Sutton, Mon. Not. R. Astron. Soc. 397, 634 (2009).
4B. P. Crill, P. A. R. Ade, E. S. Battistelli, S. Benton, R. Bihary, J. J. Bock, J. R. Bond, J. Brevik, S. Bryan, C. R. Contaldi, O. Doré, M. Farhang, L. Fissel, S. R. Golwala, M. Halpern, G. Hilton, W. Holmes, V. V. J. Hubmayr, A. Jaffe, B. Johnson, T. Jones, J. Klein, A. Korotkov, S. Leach, A. Lee, L. Levinson, M. Limon, J. Macaluso, K. MacDermid, T. Matsumura, X. Meng, A. Miller, M. Milligan, E. Pascale, D. Polsgrove, N. Ponthieu, B. Reichborn-Kjennerud, T. Renbarger, I. Sagiv, F. Strivoli, R. Stompor, H. Tran, G. Tucker, J. Vinokurov, M. Zaldarriaga, and K. Zilic, Proc. SPIE 7020, 70202N (2008).
5W. F. Grainger, P. A. R. Ade, P. Hargrave, S. Chase, B. Kieman, and C. E. North, Proc. SPIE 7739, 773916 (2010).
6L. P. Grishchuk, Sov. J. Exp. Theor. Phys. 40, 409 (1974).
7W. Hu, M. M. Hedman, and M. Zaldarriaga, Phys. Rev. D 67(4), 043004 (2003).
8M. Kamionkowski, A. Kosowsky, and A. Stebbins, Phys. Rev. Lett. 78, 2658 (1997).
9E. Komatsu, K. M. Smith, J. Dunkley, C. L. Bennett, B. Gold, G. Hinshaw, N. Jarosik, D. Larson, M. R. Poltza, L. Page, D. N. Spergel, M. Halpern, R. S. Hill, A. Kogut, M. Limon, S. S. Meyer, N. Odegard, G. S. Tucker, J. L. Weiland, E. Wollack, and E. L. Wright, ApJS 192, 18 (2011).
10J. Lagarias, J. Reeds, M. Wright, and P. Wright, SIAM J. Optim. 9, 1192 (1998).
11J. M. Lamarre, J. L. Puget, F. Bouchet, P. A. R. Ade, A. Benoit, J. P. Bernard, J. Bock, P. de Bernardis, J. Charr, F. Couchot, J. Delabrouille, G. Efstathiou, M. Giard, G. Guyot, A. Lange, B. Maffei, A. Murphy, F. Pajot, M. Piat, I. Ristorcelli, D. Santos, R. Sudilova, J. F. Sygnet, J. P. Torre, Y. Yurchenko, and D. Yvon, New Astron. Rev. 47, 1017 (2003).
12A. T. Lee, H. Tran, P. Ade, K. Arnold, J. Borrill, M. A. Dobbs, J. Errard, N. Halverson, W. V. Holzapfel, J. Howard, A. Jaffe, B. Keating, Z. Kermish, E. Linder, N. Miller, M. Myers, A. Niarchou, H. Paar, C. Reichardt, H. Spieler, B. Steinbach, R. Stompor, C. Tucker, E. Quealy, P. L. R. Richards, and O. Zahn, AIP Conf. Proc. 1040, 66 (2008).
13A. Lewis, A. Challinor, and A. Lasenby, Astrophys. J. 538, 473 (2000).
14N. Mandolesi, M. Bersanelli, R. C. Butler, E. Artal, C. Baccigalupi, A. Balbi, A. J. Banday, R. B. Barreiro, M. Bartelmann, K. Bennett, P. Bhandari, A. Baloldi, J. Borrill, M. Bremer, C. Burigana, R. C. Bowman, P. Cabella, C. Cantalupo, C. Baccigalupi, T. P. Choudhury, P. Choudhury, G. Font, G. Franceschi, G. Fratelli, P. Frailis, E. Franceschi, J. T. Gaier, S. Galeotta, F. Gasparo, G. Giardino, F. Gomez, J. Gonzalez-Nuevo, K. M. Gorski, A. Gregorio, A. Gruppuso, F. Hansen, M. Halpern, R. Hell, D. Herranz, J. M. Herreros, S. Hildebrandt, W. Hovest, R. Hoyland, K. Huffenberger, M. Janssen, T. Jaffe, E. Keihänen, R. Keski-Kupiainen, S. Lähteenmäki, C. Lawrence, S. Leach, J. P. Leahy, R. Leonardi, S. Levin, P. B. Lilje, M. López-Camn-Toledo, S. R. Lowe, P. M. Lubin, D. Maino, M. Malaspina, M. Maris, J. Marti-Canales, E. Martinez-Gonzalez, M. Massardi, S. Matarrese, F. Matthai, M. Meinhold, A. Melchiorri, L. Mendes, A. Mennella, G. Morgante, G. Moro, M. Morisset, A. Moss, A. Nash, P. Notari, R. Nester, C. Paine, B. Partridge, J. Pasian, T. Passvogel, D. Pearson, L. Pérez-Cuevas, C. Perrotta, G. Polenta, L. A. Popa, L. Pozzo, G. Prezeau, M. Prima, J. P. Rachen, R. Reboleo, M. Reinecke, S. Ricciardi, T. Riffer, G. Rocha, N. Roddis, R. Röhlfs, J. A. Rubio-Martin, E. Salerno, M. Sandri, D. Scott, M. Seiffert, J. Silk, A. Simonett, G. F. Sloom, C. Sozi, J. Sternberg, F. Stivoli, L. Stringhetti, J. Tauber, L. Terenzi, M. Tomasi, J. Tuovinen, L. White, W. White, S. White, A. Wilkinson, A. Zacchei, and A. Zonca, A&A 520, 3 (2010).
15E. C. North Ph.thesis, University of Oxford, 2010.
16See http://healpix.jpl.nasa.gov for the healpix software and full documentation.
17V. A. Rubakov, M. V. Sazhin, and A. V. Veryaskin, Phys. Lett. B 115, 189 (1982).
18See http://healpix.jpl.nasa.gov for the healpix software and full documentation.
19C. Bischoff et al., e-print arXiv:1012.3191 (http://adsabs.harvard.edu/abs/2010arXiv1012.3191Q).
20A. A. Starobinski, Sov. Astron. Lett. 9, 302 (1983).
21A. A. Starobinsky, Phys. Lett. B 117, 175 (1982).
22B. Ung and Y. Sheng, Opt. Express 15(3), 1182 (2007).
23M. Zaldarriaga and U. Seljak, Phys. Rev. D 55, 1830 (1997).