The conundrum of functional brain networks: small-world efficiency or fractal modularity

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1. INTRODUCTION

The human brain has been studied at multiple scales, from neurons, circuits, areas with well-defined anatomical and functional boundaries, to large-scale functional networks which mediate coherent cognition. In a recent work, we addressed the problem of the hierarchical organization in the brain through network analysis. Our analysis identified functional brain modules of fractal structure that were interconnected in a small-world topology. Here, we provide more details on the use of network science tools to elaborate on this behavior. We indicate the importance of using percolation theory to highlight the modular character of the functional brain network. These modules present a fractal, self-similar topology, identified through fractal network methods. When we lower the threshold of correlations to include weaker ties, the network as a whole assumes a small-world character. These weak ties are organized precisely as predicted by theory maximizing information transfer with minimal wiring costs.

Keywords: fractal networks, brain functional networks, small-world, modularity, percolation, fMRI

The functional magnetic resonance imaging (fMRI) technique is a tool that has greatly improved our ability to probe brain activity. The method detects changes in blood oxygenation when areas of the brain are activated and consequently require increased blood flow. In this way, we can monitor what brain areas respond to different mental activities. The resulting datasets offer a threedimensional image of the brain indicating the level of activation at various regimes.

Many methods have been applied to analyze fMRI data, ranging from statistics to signal processing techniques. Recently, the brain organization has been described as a complex network (Eguiluz et al., 2005; Sporns et al., 2005; Bullmore and Sporns, 2009). This approach can take various forms, such as physical connections between neurons or correlations in the activity between brain areas at a coarser level. In a recent work (Gallos et al., 2012) we used recent advances in fractal network theory to characterize the brain clusters structure, and studied one key problem of neuroscience, namely the integration of modular clusters in a larger scale. Here, we expand on those findings and describe the methodology in detail, focusing on the use of network theory in the study of fMRI data.

One of the main features of our sensations is its unitary nature. The brain can receive many concurrent stimuli. These have to be processed independently of each other, but at the same time they have to be integrated into a unified entity. This suggests that the modalities in the brain that process different characteristics have to act isolated for efficient computations, but they need also be sufficiently connected in order to perform coherent functions.

The notion of a complex network can be suitably adapted to address this scaling problem and study optimal information flow in modular networks. This representation of complicated interactions has offered new insight in many processes across different disciplines. A key feature of many such networks is their modular character, a topic which has attracted a lot of interest in the literature. Many algorithms have been proposed for the detection of modules, loosely defined as network areas well-connected within themselves but sparsely connected to the rest of the network. The detection and behavior of modules at different observation scales, though, remains a largely unexplored problem. Network analysis of functional (Eguiluz et al., 2005) and structural (Sporns et al., 2005) data has been used to characterize global connectivity and topological organization of the human brain (Bullmore and Sporns, 2009). Many of those studies indicate the small-world character (Watts and Strogatz, 1998) of brain networks, but the idea of a simple small-world structure can be contradictory to modular network.

In the present manuscript we implement a complex network analysis to understand the hierarchical organization of functional brain networks, and we study how we can explain the emergence of both small-world and modular features in the same network. We capitalize on a well known dual-task paradigm, the psychological refractory period, in which information from different sensory modalities (visual and auditory) has to be coherently routed to different motor effectors (in this experiment, the left and right-hand).

The combination of high-temporal resolution fMRI with novel network analysis tools allows the study of the module properties and their synergy toward accomplishing a cognitive task. A functional correlation network is derived from the fMRI phase information. We implement percolation and scaling analysis methods to uncover a highly modular functional operation and a network that is almost optimally connected for efficient information flow.
2. MATERIALS AND METHODS

2.1. EXPERIMENTAL DESIGN

We use time-resolved fMRI (Menon et al., 1998), based on analysis of the phase signal (Sigman et al., 2007). Time-resolved fMRI is capable of identifying the series of processing stages which unfold sequentially during the execution of a compound dual-task (Dux et al., 2006; Sigman and Dehaene, 2008).

The details of the experiments are described in Sigman et al. (2007), and are briefly reviewed here. Sixteen participants performed a dual-task paradigm: first a visual task of comparing an Arabic numeral (target T1) to a fixed reference, with a right-hand response and, second, an auditory task of judging the pitch of an auditory tone (target T2) with a left-hand response. The stimulus onset asynchrony (SOA) between T1 and T2 was varied between 0, 300, 900, and 1200 ms. In the course of this analysis we did not detect significant differences in the resulting patterns of different SOA conditions.

While subjects performed the dual-task, whole-brain fMRI images were recorded at a sampling time (TR) of 1.5 s, and subsequently the phase and amplitude of the hemodynamic response were computed (Sigman et al., 2007). This activated map exhibits phases consistently falling within the expected response latency for a task-induced activation. As expected for an experiment involving visual and auditory stimuli and bimanual responses, the responsive regions included bilateral visual occipito-temporal cortices, bilateral auditory cortices, motor, premotor and cerebellar cortices, and a large-scale bilateral parieto-frontal network (Sigman and Dehaene, 2008). In this study we try to understand the topology of the modular organization of this broad functional network during dual-task performance. For this purpose, we derived a large functional network of brain areas by measuring the phase correlations in these responses for all pairs of voxels. We then connected the highly correlated pairs which gave us the brain cluster network structure.

2.2. PHASE CORRELATIONS AND FUNCTIONAL BRAIN NETWORK

We use network theory concepts for the analysis of correlations between different brain areas, based on the temporal activation of these areas when a subject responds to external stimuli. We reconstruct the network topology of brain voxels, where a network link indicates a high correlation in the phase-space activity of the two connected voxels, and compare this structure with the corresponding topology of the voxel location in the brain.

The time evolution of the phase of all brain voxels over 440 s was recorded for each participant and each of the four SOA conditions, for a total of 64 measurements. For our analysis, we create a mask where we only keep voxels which were activated in more than 75% of the cases, i.e., in at least 48 instances.

We want to detect the correlation between the phases of two voxels i and j in the activated mask. The measure of correlation for vectors is the co-directionality, i.e., we need to calculate the angle between the two vectors. Therefore, the correlation rij between two vectors \( \vec{r}_i \) and \( \vec{r}_j \) is given, in general, by

\[
rij = \frac{\vec{r}_i \cdot \vec{r}_j}{|\vec{r}_i||\vec{r}_j|},
\]

which is equivalent to the cosine of the included angle, i.e.,

\[
rij = \cos(\theta),
\]

where \( \theta \) is now the phase difference \( a_i - a_j \). We average the correlation between any two voxels i and j in the activated mask over roughly 40 trials of each experiment. The resulting correlation \( p_{ij} \) between these two voxels is then given by

\[
p_{ij} = \frac{1}{N} \sum_{t=1}^{N} \cos \left[ a_i(t) - a_j(t) \right],
\]

where \( N \) is the number of trials for a given combination of subject and stimulus. We link two voxels if their correlation is larger than a threshold value \( p \). The resulting network is a representation of functional relations among voxels for a specific subject and stimulus.

The topology of this network strongly depends on the value of \( p \). The variation of \( p \) describes a percolation process. A large \( p \)-value enables isolated module identification, since only the strongest (i.e., more correlated) functional links between voxels are preserved. As \( p \) is lowered, these modules get progressively merged to larger entities and the emphasis is shifted toward large-scale properties of the spanning network.

The complex network representation (Figure 1A) reveals functional links between brain areas, but cannot directly reveal spatial correlations. Since voxels are embedded in space, we also study the topological features of spatial clusters in three-dimensions, where now voxels assume their known positions in the brain and links between them are transferred from the corresponding network (Figure 1B), i.e., they are assigned according to the degree of correlation between any two voxels, independently of the voxels proximity in real-space.

The above procedure yields a different network or spatial clusters for each subject. We study each of those networks and clusters separately and show that they all carry statistically similar properties. For efficiency purposes, we focus our attention to the case of the largest \( p_c \) value where three clusters, including at least 1000 voxels, emerge in each trial. The spread of the corresponding \( p_c \) values is small, demonstrating a similar behavior in the brain response of different subjects.

2.3. FRACTAL ANALYSIS

We analyze the resulting networks and the embedded three-dimensional clusters in terms of their fractal and modular properties. For the spatial representation, we characterize the fractality of a connected cluster through the standard Hausdorff dimension \( d_f \). Starting from an arbitrary point in a cluster, \( d_f \) measures how the mass \( N_f \) (number of voxels in the same cluster) scales with the Euclidean distance \( r \) from this origin, i.e.,

\[
N_f(r) \sim r^{d_f}.
\]

The exponent \( d_f \) shows how densely the area is covered by a specific cluster.

The box-covering technique is used for the fractal analysis of the complex networks. A network (in our case each cluster) is first tiled with the minimum possible number of boxes, \( N_{B} \), of a given size \( \ell_B \). A box is defined as a union of nodes, all of which are at a distance from each other smaller than a given threshold length, the box size \( \ell_B \) (the distance between two nodes, \( \ell \), is defined as the number of links along the shortest path between those nodes in the functional brain network).
The fractality (self-similarity) of the network is quantified in the power-law relation between the number of boxes needed to cover the network and the box size $\ell_B$:

$$N_B(\ell_B) = N_0 \ell_B^{-d_B},$$

where $d_B$ is the fractal dimension (or box dimension) and $N_0$ is the number of nodes in the original network (Song et al., 2005a, 2006; Goh et al., 2006; Kim et al., 2007; Radicchi et al., 2008). Finite and small values of $d_B$ show that the network has fractal features, where the covering boxes retain their connectivity scheme under different scales, and larger-scale boxes behave in a similar way as the original network.

The requirement that the number of boxes should be minimized poses an optimization problem which can be solved using a number of box-covering algorithms. The method that we implement here is called Maximum Excluded Mass Burning algorithm (MEMB), and the algorithm can be downloaded from http://lev.ccny.cuny.edu/hmakse/soft_data.html). The method is roughly explained in Figure 2. The detection of modules or boxes in our work follows from the application of this algorithm (Song et al., 2005a, 2007) at different length-scales.

The MEMB method starts by determining the minimum number of boxes of radius $r_B$ required for a complete coverage of the network. This radius is the distance from a box “center,” so that by definition all nodes in a box are within a distance from each other smaller than $\ell_B = 2r_B + 1$. The method detects the nodes that will act as the centers of the boxes, by calculating the mass around each node if it would act as a center. The node with maximum mass around it is selected as a center and we proceed iteratively to find the minimum number of such centers. Once these nodes have been determined, the boxes are built by including successive layers of nodes around the centers. The details of the method are reported in Song et al. (2007).

The resulting boxes are characterized by the proximity between all their nodes, at a given length-scale and the maximization of the mass associated with each module center. Thus, MEMB detects boxes that also tend to maximize modularity. Different values of the box diameter $\ell_B$ yield boxes of different size. These boxes are then identified as modules which at a smaller scale $\ell_B$ may be separated, but merge into larger entities as we increase $\ell_B$. Thus, we can study the hierarchical character of modularity, i.e., modules of modules, and we can detect whether modularity is a feature of the network that remains scale-invariant.

For this, we can extend the box-covering concept to act as a community detection algorithm (Galvao et al., 2010). MEMB identifies modules of size $\ell_B$, composed of highly connected brain areas. Typical modularity approaches do not place constraints on the size of the modules, but they focus on minimizing the number of inter-module links. The MEMB approach, though, has the additional advantage that modularity can be studied at different scales. The requirement of minimal number of modules to cover the network ($N_B$) guarantees that the partition of the network is such that each module contains the largest possible number of nodes and links inside the module with the constraint that the modules cannot exceed size $\ell_B$. This optimized tiling process gives rise to modules with the fewest number of links connecting to other modules. This implies that the degree of modularity for a given $\ell_B$ value is maximized, and we can define a modularity.
We use percolation theory (Bunde and Havlin, 1996) to identify the modular structure in the network. They indicate that at any given p-value there are many isolated clusters in the brain network, which subsequently merge into the largest cluster as p decreases. This is a universal behavior observed in all participants, and allows the identification of functional modules, which we proceed to study next.

The clusters identified by percolation analysis at a given threshold p are functionally connected, but the nodes in such a cluster are not necessarily clustered in space. Thus, we first studied whether the percolation clusters had a consistent spatial projection. The p-values at which clusters appear varied across participants. To group the data, we measured, for each participant, the highest correlation p-value for which there were at least three clusters of 1000 voxels each. The topography of these clusters reflected coherent patterns across different individuals. In virtually all participants we observed a cluster covering the premotor, supplementary motor area (SMA) region, a cluster covering the medial part of the posterior parietal cortex (PPC) and a cluster covering the medial part of early retinotopic cortex (area V1), along the calcarine fissure.

We then measured the likelihood that a voxel may appear in a percolation cluster, by counting, for each voxel, the number of individuals for which it was included in one of the first three percolation clusters (Figure 4).

Clusters in the three main nodes, V1, SMA, PPC, are ubiquitously present in percolation clusters and, to a lesser extent, voxels in the motor cortex (along the central sulcus) slightly more predominantly on the left hemisphere.

This analysis demonstrated that the correlation networks obtained from each subject yielded percolation clusters with consistent topographic projections. Next we focus on our main aim; exploring the topology and scaling properties of the network modules using fractal network analysis.

3.2. Fractal Analysis Results

For each of the 16 participants and each of the 4 SOA conditions we calculated the resulting network through the phase correlation. Then, for each network, we estimated the percolation threshold that yields three clusters of at least 1000 voxels each. This results in a total of 192 clusters which were pooled together for the present analysis.

We applied the box-covering algorithm (Song et al., 2005a, 2007) to measure the fractal dimension $d_B$ of these 192 clusters. The fractal dimension $d_B$ was calculated separately for each cluster. The resulting network fractal dimensions were distributed in a relatively narrow range, with an average value $d_B = 1.9 \pm 0.1$ (Figure 5A).

The cluster structure can be also probed by its topological features when every node-voxel assumes its assigned location at the brain. Each cluster identified by the box-covering algorithm can be mapped to their anatomical projections, where two voxels are still connected according to their correlation but their distance is now defined by the Euclidean three-dimensional spatial distance.
FIGURE 3 | (A) Bond percolation in a 2-dimensional lattice. We remove a random bond with probability \( p \), and with probability \( 1 - p \) a bond remains (denoted by a solid black line). The lattice with solid black bonds is at the percolation transition \( p = p_c \). (B) Evolution of modules at different thresholds. The size of the three largest clusters as a function of the correlation threshold \( p \) for a given subject. As we lower \( p \), the cluster size increases in jumps, and new clusters emerge, grow, and finally get absorbed by the largest cluster. This behavior is significantly different from the random percolation in (A). (C) Cluster evolution. Brain clusters with more than 1000 voxels, as identified through correlation analysis for a given \( p \)-value.

The method that we use to calculate the fractal dimension here is an alternative method to the one used in Gallos et al. (2012). There, \( d_f \) was calculated by measuring the number of nodes, \( N_{CC} \), in a cluster as a function of the cluster diameter. Here, for every cluster we start from a random point and open a circle of radius \( r \) and measure the number of nodes \( N_f(r) \) in this circle. The dependence of \( N_f(r) \) on \( r \) for this cluster gives its fractal dimension, and the process is repeated for all clusters. The scaling of the mass \( N_f(r) \) (i.e., number of nodes in the cluster) included in a sphere with Euclidean radius \( r \) follows the power-law form of equation (2). The calculation of the individual Euclidean fractal dimensions yields an average of \( d_f = 2.1 \pm 0.1 \) (Figure 5B), which is similar for all clusters, and which is exactly the same as the one found in Gallos et al. (2012). The network fractal dimension of all clusters was systematically lower than the real-space fractal dimension, which was in the range 2–2.4.

It is possible that the difference between the fractal dimensions of individual clusters can be due to systematic variations, influenced by various factors. We performed a number of tests to identify the stability of these calculations. In Figure 6A we show a cross-plot for the exponents \( d_B \) and \( d_f \) as calculated for each individual cluster. The value of \( d_B \) was systematically below \( d_f \). From the same plot we deduce that the value of the percolation
FIGURE 4 | The emerging clusters have consistent spatial projections. (A) The color denotes the fraction of the total number of voxels that appear to one of the three largest clusters in N subjects at a given percolation threshold p. As we reduce the threshold the peak shifts toward larger N values, i.e., the same voxels appear consistently in the largest clusters for all subjects. (B,C) Spatial distribution of the first percolation clusters (in subject counts). The two brain slices show for the highest p-values the shared voxels. White bleached regions correspond to voxels which are included in the first percolation cluster for all subjects. The SMA, a region involved in planning motor action is the only shared region for all subjects.

FIGURE 5 | (A) Fractal dimension $d_B$ of the network clusters. The line is representative of the average dimension $d_B = 1.9$. (B) Fractal dimension $d_f$ of the spatially embedded clusters. The large points represent the number of nodes $N_f(r)$ included within a fixed distance $r$, averaged over all clusters, while smaller points refer to individual clusters. The fitted line corresponds to the average dimension $d_f = 2.1$.

transition does not influence the fractal dimension, since the different $p_c$ values of different clusters yield a uniform spreading of the fractal dimensions. It is also possible that the location of the brain clusters may have an effect on their fractal character. Our results do not provide any evidence toward this direction, either. In Figure 6B we plot the exponents $d_B$ and $d_f$ for each cluster as
a function of the $y$-coordinate of the cluster’s center of mass, i.e., increasing $y$ indexes corresponds to moving from the posterior to the anterior part of the brain. It is obvious that there is no systematic variation of the exponents in different locations. The above results emphasize the robustness of the fractal structure and indicate that we can consider the averages over all those structures to be representative of a typical brain module.

We can now characterize each single cluster, both at the functional level and at the topological level (i.e., the shape that the cluster assumes in the brain). Together, these results indicate that none of the clusters fill the 3D space densely; although the objects are embedded in three-dimensions their fractal dimension $d_f$ is significantly smaller than 3. The network structure provides information on functional clusters, since it relates areas that are highly correlated independently of their physical proximity. Since the network fractal dimension $d_B$ is even smaller than $d_f$, connections are fewer than one would expect through nearest-neighbor connections only. In simpler words, clusters do not form densely connected neighborhoods.

### 3.3. MODULAR STRUCTURE

In the Materials and Methods section we described how we can use the optimal MEMB coverage of the network with $N_B$ nodes for a given $\ell_B$ value, in order to characterize the network modularity. Analysis of the modularity equation (4) in Figure 7 reveals a monotonic increase of $M(\ell_B)$ with a lack of a characteristic value of $\ell_B$. Indeed, the data can be approximately fitted with a power-law functional form, equation (5), which is characterized by the modularity exponent $d_M$. We analyze the resulting networks of different subjects and we find that $d_M = 1.9 \pm 0.1$ is approximately constant over different individuals (Figure 7).

This value reveals a considerable degree of modularity in the entire system as evidenced by the network structure. For comparison, a random network has $d_M = 0$ and a uniform lattice has $d_M = 1$ (Gallos et al., 2007). The lack of a characteristic length-scale in the modularity shown in Figure 7 suggests that the modules appear at all length-scales, i.e., modules are organized within larger modules in a self-similar way, so that the inter-connections between those clusters repeat the basic modular character of the entire brain network. Thus, the modular organization of the network remains statistically invariant when observed at different scales.

### 3.4. SHORT-CUT WIRING IS OPTIMIZED FOR EFFICIENT FLOW

A major advantage of the present analysis approach is that the analysis of the type of short-cuts present in the brain networks can convey a notion of optimal navigability in the network.

The addition of long-range links can turn the balance of a network structure toward either a self-similar structure with significant modularity but poor transfer or toward a small-world structure with very efficient flow at the cost of modularity (specialization). A small number of such short-cuts, quantified through renormalization group analysis (Rozenfeld et al., 2010), has been shown to provide the optimal trade-off between these two properties. In the case of the brain clusters the need for specialization/modularity is obvious, as also shown in the previous section,
so it is important to understand how short-cuts influence the efficiency of signal transport in these structures.

In order to study how the modules that we recovered by the first percolation transition integrate at a larger scale, we also considered another percolation transition that corresponds to the emergence of a spanning cluster. We chose this transition as the correlation point where the largest cluster is equal to half of the total size. This global network connects practically all the smaller brain modules.

We probed the connectivity for this network, by analyzing the distance distribution of the links in the network, i.e., the Euclidean distance between any two voxels that are connected through their phase correlation (Figure 8A). We find an approximately power-law distribution (Figure 8B) of the form:

\[ P(r) \sim r^{-\alpha}, \]

with a short-cut exponent \( \alpha \approx 3.1 \). The value of this exponent is very significant, since it approximately satisfies the scaling relation with the fractal dimension of the brain network:

\[ \alpha = d_f + 1. \]

Such a scaling relation was recently (Li et al., 2010) found to optimize the transfer of information across a network with fractal dimension \( d_f \) when the short-cuts in the network are added with a cost constraining the number of total links. Thus, our scaling and modular analysis suggests that, taking into account the spatial restrictions, the functional behavior of the brain is optimally wired for facilitating efficient information transfer among different areas.

4. DISCUSSION

Our analysis revealed a fractal structure for the individual brain clusters. These clusters have a consistent topological behavior and are located at the areas that correspond to the expected brain responses. These modular structures present consistent fractal properties, both at the functional level and at a topological level. This indicates that the individual processing units that we recover do not have significant small-world properties. In contrast, when we include weaker correlations, the modules that appear at smaller scales are connected through long-range links. These short-cuts give a small-world character to the brain network as a whole, i.e., when studied at scales larger than an individual module.

The study of the distribution for these links suggests interestingly that they are optimizing transfer network properties, by also considering the wiring cost. In simpler terms, this topology does not minimize the global connectivity, simply to connect all the nodes; instead it minimizes the amount of wire required to achieve the goal of shrinking the network to a small-world.

The existence of modular organization of strong ties in a sea of weak ties is reminiscent of the structure found to bind dissimilar communities in social networks. Granovetter’s (1973) work in social sciences proposes the existence of weak ties to cohere well-defined social groups into a large-scale social network. Such a two-scale structure has a large impact on the diffusion and influence of information across the entire social structure. Our observation of this two-layer organization in brain networks suggests that it may be a ubiquitous natural solution to the puzzle of information flow in highly modular structures.

Previous studies have found that wiring of neuronal networks at the cellular level is close to optimal (Song et al., 2005b). Specifically it is found that long-range connections do not minimize wiring but achieve network benefits. In agreement with this observation, at the mesoscopic scale explored here, we find an optimization which reduces wiring cost while maintaining network proximity. An intriguing element of our observation is that this minimization assumes that broadcasting and routing information are known to each node. How this may be achieved – what aspects of the neural code convey its own routing information – remains an open question in Neuroscience.
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