Evidence for $B^- \to \tau^- \nu_\tau$ with a Semileptonic Tagging Method

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We present a measurement of the decay $B^- \to \tau^- \nu_{\tau}$ using a data sample containing $657 \times 10^6$ $B\bar{B}$ pairs collected at the $\Upsilon(4S)$ resonance with the Belle detector at the KEKB asymmetric-energy $e^+e^-$ collider. A sample of $B^+B^-$ pairs are tagged by reconstructing one $B^+$ meson decaying semileptonically. We detect the $B^- \to \tau^- \nu_{\tau}$ candidate in the recoil. We obtain a signal with a significance of 3.6 standard deviations including systematic uncertainties, and measure the branching fraction to be $\mathcal{B}(B^- \to \tau^- \nu_{\tau}) = [1.54^{+0.32}_{-0.31}(\text{stat})^{+0.29}_{-0.31}(\text{syst})] \times 10^{-4}$. This result confirms the evidence for $B^- \to \tau^- \nu_{\tau}$ obtained in a previous Belle measurement that used a hadronic $B$ tagging method.

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The purely leptonic decay $B^- \to \tau^- \nu_{\tau}$ is of particular interest since it provides a unique opportunity to test the Standard Model (SM) and search for new physics beyond the SM. In the SM, the branching fraction of the decay $B^- \to \tau^- \nu_{\tau}$ is given by

$$\mathcal{B}(B^- \to \tau^- \nu_{\tau}) = \frac{G_F^2 m_B m_{\tau}^2}{8\pi} \left(1 - \frac{m_{\tau}^2}{m_B^2}\right)^2 f_B^2 |V_{ub}|^2 \tau_B,$$

where $G_F$ is the Fermi coupling constant, $m_{\tau}$ and $m_B$ are the $\tau$ lepton and $B^-$ meson masses, $\tau_B$ is the $B^-$ lifetime, $|V_{ub}|$ is the magnitude of the Cabibbo-Kobayashi-Maskawa (CKM) matrix element, and $f_B$ is the $B$ meson decay constant. Dependence on the lepton mass arises from helicity conservation, which suppresses the muon and electron channels. A recent SM estimation of the branching fraction is $(0.76^{+0.11}_{-0.09}) \times 10^{-4}$. In the absence of new physics, measurement of the $B^- \to \tau^- \nu_{\tau}$ decay can provide a direct experimental determination of $f_B$, which can be compared to lattice QCD calculations.

Physics beyond the SM, however, could significantly suppress or enhance $\mathcal{B}(B^- \to \tau^- \nu_{\tau})$ via exchange of a new charged particle such as a charged Higgs boson from supersymmetry or two-Higgs doublet models.

Belle previously reported the first evidence of $B^- \to \tau^- \nu_{\tau}$ decay with a significance of 3.5 standard deviations, and measured the branching fraction to be $\mathcal{B}(B^- \to \tau^- \nu_{\tau}) = (1.79^{+0.56}_{-0.49}(\text{stat})^{+0.45}_{-0.51}(\text{syst})) \times 10^{-4}$, using a hadronic reconstruction tagging method. The BaBar Collaboration reported a search for $B^- \to \tau^- \nu_{\tau}$ decay with hadronic tagging using $383 \times 10^6$ $B\bar{B}$ pairs and with semileptonic tagging using $459 \times 10^6$ $B\bar{B}$ pairs. Combining the two measurements, they obtained a $2.8\sigma$ excess and a branching fraction $\mathcal{B}(B^- \to \tau^- \nu_{\tau}) = (1.7 \pm 0.6) \times 10^{-4}$. These experimental results are slightly larger than the SM estimation in Ref. 2, though the statistical precision is not sufficient to demonstrate the existence of physics beyond the SM. To better establish this decay mode and determine the branching fraction with greater precision, we present a measurement of $B^- \to \tau^- \nu_{\tau}$ from Belle using a semileptonic tagging method.

We use a $605 \text{ fb}^{-1}$ data sample containing $657 \times 10^6$ $B\bar{B}$ pairs collected with the Belle detector at the KEKB asymmetric-energy $e^+e^-$ collider $(3.5$ on $8 \text{ GeV})$ collider operating at the $\Upsilon(4S)$ resonance ($\sqrt{s} = 10.58 \text{ GeV}$). We also use a data sample of $68 \text{ fb}^{-1}$ taken at a center of mass energy $60 \text{ MeV}$ below the nominal $\Upsilon(4S)$ mass (off-resonance) for background studies. The Belle detector is a large-solid-angle magnetic spectrometer that consists of a silicon vertex detector (SVD), a 50-layer central drift chamber (CDC), an array of aerogel threshold Cherenkov counters (ACC), a barrel-like arrangement of time-of-flight scintillation counters (TOF), and an electromagnetic calorimeter (ECL) comprised of CsI(Tl) crystals located inside a superconducting solenoid coil that provides a 1.5 T magnetic field. An iron flux-return located outside of the coil is instrumented to detect $K_L^0$ mesons and to identify muons (KLM). Two inner detector configurations were used. A 2.0 cm beampipe and a 3-layer silicon vertex detector were used for the first sample of $152 \times 10^6 B\bar{B}$ pairs, while a 1.5 cm beampipe, a 4-layer silicon detector and a small-cell inner drift chamber were used to record the remaining $505 \times 10^6 B\bar{B}$ pairs.

We use a detailed Monte Carlo (MC) simulation based
on GEANT to determine the signal selection efficiency and study the background. In order to reproduce the effects of beam background, data taken with random triggers for each run period are overlaid on simulated events. The $B^- \to \tau^- \pi_\tau$ signal decay is generated by the EvtGen package. Radiative effects are modeled using the PHOTOS code. To model the background from $e^+e^- \to BB$ and continuum $q\bar{q}$ ($q = u, d, s, c$) production processes, we use large MC samples of $BB$ meson pair decays to charm and continuum $q\bar{q}$ processes corresponding to about ten times and six times the data sample, respectively. We also use MC samples of rare $B$ decay processes such as charmless hadronic, radiative, electroweak decays and $b \to u$ semileptonic decays. The contamination from other low multiplicity backgrounds such as $e^+e^- \to \tau^+\tau^-$ and two-photon processes is also studied using dedicated MC samples.

The $B^- \to \tau^- \pi_\tau$ candidate decays are selected using the feature that at the $\Upsilon(4S)$ resonance $B$ meson pairs are produced with no additional particles. We first reconstruct one of the $B$ mesons decaying semileptonically (referred to hereafter as $B_{\text{tag}}$) and then compare the properties of the remaining particle(s) in the event ($B_{\text{sig}}$) to those expected for signal and background. In order to avoid experimental bias, the signal region in data is not examined until the event selection criteria are finalized.

Charged particles are selected from well measured tracks (reconstructed with the CDC and SVD) originating from the interaction point. Electron candidates are identified based on a likelihood calculated using the following information: $dE/dx$ measured in the CDC, the response of the ACC, the ECL shower shape and the ratio of the ECL energy deposited to the track momentum. Muon candidates are selected using KLM hits associated to a charged track. Both muons and electrons are selected with efficiency greater than 90% in the momentum region above 1.2 GeV/c, and misidentification rates of less than 0.2% (1.5%) for electrons (muons). After selecting leptons, we distinguish charged kaons from pions based on a kaon likelihood derived from the TOF, ACC, and $dE/dx$ measurements in the CDC. The typical kaon identification efficiency is greater than 85% and the probability of misidentifying pions as kaons is about 8%. Photons are identified as isolated ECL clusters that are not matched to any charged track. Neutral $\pi^0$ candidates are selected from pairs of photons with invariant mass between 0.118 and 0.150 GeV/c$^2$. The energy of the photon candidates must exceed: 50 MeV for the barrel, 100 MeV for the forward endcap and 150 MeV for the backward endcap, except for low momentum $\pi^0$ candidates from $D^0 \to D^0 \pi^0$ decay for which we require the photon energy to be greater than 30 MeV.

We reconstruct the $B_{\text{tag}}$ in $B^+ \to D^0 \ell^+ \nu_\ell$ and $B^+ \to \overline{D}^0 \ell^+ \nu_\ell$ decays, where $\ell$ is electron ($e$) or muon ($\mu$). $D^0$ mesons are reconstructed in the $K^+\pi^-$, $K^+\pi^+\pi^0$ and $K^+\pi^+\pi^-\pi^0$ modes. For $B_{\text{sig}}$, we use $\tau^-$ decays to only one charged particle and neutrinos i.e. $\tau^- \to \ell^- \nu_\ell \tau$ and $\tau^- \to \pi^- \nu_\tau$. We require the invariant mass of $D^0$ candidates to be in the range [1.851 GeV/c$^2$, 1.879 GeV/c$^2$] for $D^0 \to K^+\pi^-$ and $K^+\pi^-\pi^+\pi^-$ decays, and [1.829 GeV/c$^2$, 1.901 GeV/c$^2$] for $D^0 \to K^+\pi^-\pi^0$ decay. $D^0$ candidates are selected by combining the $D^0$ candidates with low momentum $\pi^0$ candidates or photons. For $D^0$ candidates, we require the mass difference $\Delta M = M_{D\pi^0} - M_{D^0}$ to be in the range [0.1389 GeV/c$^2$, 0.1455 GeV/c$^2$] and [0.123 GeV/c$^2$, 0.165 GeV/c$^2$] for $D^0 \to D^0 \pi^0$ and $D^0 \to D^0 \gamma$ decays, respectively. These regions correspond to three standard deviations in the corresponding resolutions. To suppress $D^0$’s from continuum background processes, the momentum of $D^0$ candidates calculated in the $\Upsilon(4S)$ center-of-mass system (cms) is required to be less than 2.5 GeV/c.

We select signal candidates from events with one $D^0$ or $\overline{D}^0$ and one $\ell^+$ to form $B_{\text{tag}}$, and one $\ell^-$ or $\pi^-$ candidate for $B_{\text{sig}}$. We require that no other charged particle or $\pi^0$ remain in the event after removing the particles from the $B_{\text{tag}}$ and $B_{\text{sig}}$ candidates. The $B_{\text{tag}}$ candidates are selected using the lepton momentum in the cms frame, $P_{\text{B}}^{\text{cms}}$, and the cosine of the angle between the direction of the $B_{\text{tag}}$ momentum and the direction of the momentum sum of the $D^{(*)0}$ and the lepton, $\cos \theta_{B,D^{(*)}\ell}$, measured in the cms frame. This angle is calculated using

$$\cos \theta_{B,D^{(*)}\ell} = \frac{2 E_{\text{beam}}^{\text{cms}} E_{D^{(*)}\ell}^{\text{cms}} - m_B^2 - M_{D^{(*)}\ell}^2}{2 P_B^{\text{cms}} P_{D^{(*)}\ell}^{\text{cms}}}$$

where $E_{\text{beam}}^{\text{cms}}$ is the beam energy, $P_B^{\text{cms}}$ is the momentum of $B$ meson calculated with $P_B^{\text{cms}} = \sqrt{(E_{\text{beam}}^{\text{cms}})^2 - m_B^2}$, $E_{D^{(*)}\ell}^{\text{cms}}$, $P_{D^{(*)}\ell}^{\text{cms}}$ and $M_{D^{(*)}\ell}$ are the energy sum, momentum sum and invariant mass, respectively, of the $D^{(*)0}$ and lepton system. All parameters are calculated in the cms. Properly reconstructed $B_{\text{tag}}$ candidates are populated within the physical range $[-1, 1]$, while combinatorial backgrounds can take unphysical values. For the signal side, the $\ell^-$ or $\pi^-$ candidate from the $\tau$ decay is selected using the momentum in the cms, denoted $P_{\text{B}}^{\text{sign}}$. The signal yield is obtained by fitting the distribution of the remaining energy in the ECL, denoted $E_{\text{ECL}}$, which is the sum of the energies of ECL clusters that are not associated with particles from the $B_{\text{tag}}$ and $B_{\text{sig}}$ candidates; here the $E_{\text{ECL}}$ clusters satisfy the same minimum energy requirements as photon candidates. For signal events, $E_{\text{ECL}}$ must be either zero or a small value arising from spillover showers created by $B_{\text{tag}}$ and $B_{\text{sig}}$ particles and residual beam background hits. Therefore, signal events peak at low $E_{\text{ECL}}$. On the other hand, background events are distributed toward higher $E_{\text{ECL}}$ due to the contribu-
tion from additional particles. The selection criteria for $P_{ECL}^{\tau \ell}$, $\cos\theta_{B,D^{(*)}\ell}\nu$ and $P_{sig}^{\tau \ell}$ are optimized for each of the $\tau$ decay modes, because the background levels and the background components are mode-dependent. The optimization is done so that the figure of merit $s/\sqrt{s+n}$ is maximized, where $s$ and $n$ are the number of signal and background events expected in the signal-enhanced region $E_{ECL} < 0.2$ GeV, calculated assuming a signal branching fraction of $1.79 \times 10^{-4}$. For leptonic $\tau$ decays, the dominant background is from $B\bar{B}$ events tagged by a semileptonic decay with a correctly reconstructed combination of a $D^0$ and a $\ell^+$. For these decays lose selection criteria are chosen to maintain high signal efficiency: 0.5 GeV/c $< P_{ECL}^{\mu\nu} < 2.5$ GeV/c, $-2.1 < \cos\theta_{B,D^\ell} < 1.3$ for the $D^0$ mode or $-2.6 < \cos\theta_{B,D^\ell} < 1.2$ for the $D^0$ mode, and 0.3 GeV/c $< P_{ECL}^{\tau\ell}\nu < 1.2$ GeV/c. For the hadronic $\tau$ decay mode, there is more background from $e^+e^- \to q\bar{q}$ continuum and combinatorial $D^{(*)0}\ell$ background. Tighter criteria are used to reduce such backgrounds: 1.0 GeV/c $< P_{ECL}^{\mu\nu} < 2.2$ GeV/c, $-1.1 < \cos\theta_{B,D^{(*)}\ell}\nu < 1.1$, and 1.0 GeV/c $< P_{ECL}^{\tau\ell}\nu < 2.4$ GeV/c. The upper bound on $P_{ECL}^{\tau\ell}\nu$ is introduced to reject two-body $B$ decays. In addition, we suppress continuum background by requiring the cosine of the angle between the signal side pion track and the thrust axis of the $B_{tag}$, $\cos\theta_{thr}$, to be less than 0.9. We select candidate events in the range $E_{ECL} < 1.2$ GeV for further analysis. The number of candidate events are 2481 for $\tau^- \to e^- \pi^0\pi^0\nu_e$, 2011 for $\tau^- \to \mu^- \pi^-\nu_\mu$ and 1018 for $\tau^- \to \pi^-\nu_\pi$ decays. Figure 1 shows the $\cos\theta_{B,D^{(*)}\ell}$ distribution for the signal candidate events including both leptonic and hadronic $\tau$ decay modes with all selection criteria other than $\cos\theta_{B,D^{(*)}\ell}$ applied. The excess over the MC expectation for events without $B \to D^{(*)}\ell\nu$ decays indicates that the final sample contains candidate events with the correct combination of a $D^{(*)0}$ and a $\ell^+$ forming a $B_{tag}$. In the remaining candidates, according to a MC study, 4.6%, 13.4% and 12.0% are events without a $B_{tag}$ from $B^+ B^-$, $B^0\bar{B}^0$ and non-$B\bar{B}$ processes, respectively.

The number of signal events is extracted from an extended maximum likelihood fit to the $E_{ECL}$, distribution of the candidate events. Probability density functions (PDFs) for each $\tau$ decay mode are constructed from the MC simulation. We use $E_{ECL}$ histograms obtained from MC samples for each of the signal and the background components. The PDFs are combined into a likelihood function,

$$\mathcal{L} = \frac{e^{-\sum_i n_i}}{N!} \prod_{j=1}^{N} \sum_{j} n_j f_j(E_i)$$

(3)

where $j$ is an index for the signal and background contributions, $n_j$ and $f_j$ are the yield and the PDF, respectively, of the $j$th component, $E_i$ is the $E_{ECL}$ value in the $i$th event, and $N$ is the total number of events in the data. The dominant background components are from $B\bar{B}$ decays to a final state with charm and continuum processes. The small background from rare charmless $B$ decays and other low multiplicity processes such as $\tau$ pair and two-photon processes is also included in the fit. In the final sample with $E_{ECL} < 1.2$ GeV, the fractions of the background from rare charmless $B$ decays and low multiplicity non-$B$ processes are estimated from MC to be 8% and 3% for leptonic $\tau$ decays and 11% and 8% for hadronic $\tau$ decay, respectively.

The $E_{ECL}$ estimation in MC is validated using various control samples. The MC distributions of not only $E_{ECL}$ but also $P_{ECL}^{\tau\ell}\nu$, $\cos\theta_{B,D^{(*)}\ell}$, $P_{sig}^{\tau\ell}$ and $\cos\theta_{thr}$ are compared to those of the control samples to confirm that MC describes the background composition properly. The off-resonance data is used to calibrate the MC simulation of the continuum background. We find that our MC underestimates the overall normalization of the continuum background though the predicted shapes are consistent with data within statistical errors. We obtain the correction factor for the overall normalization of the continuum MC to be $1.43 \pm 0.11$ by comparing the number of remaining events in off-resonance data with the MC expectation. The sidebands in $\cos\theta_{B,D^{(*)}\ell}$, $D^0$ mass, the mass difference between $D^{(*)0}$ and $D^0$, and $E_{ECL}$ are used as control samples to check the overall background description including the $B\bar{B}$ contribution. The distributions in these variables obtained from MC with the continuum normalization correction applied are found to be consistent with the corresponding distributions in data.
The agreement between MC and data is also confirmed in $B^0$ tagged events where the $B_{\text{tag}}$ is reconstructed in $B^0 \rightarrow D^{*0}\ell^+\nu$ decays. The contributions to the $E_{\text{ECL}}$ distribution are not only from beam background but also include splitoff showers originating from $B_{\text{tag}}$ and $B_{\text{sig}}$ decay products. The relative fractions of these sources are 21%, 53% and 26%, respectively, in the signal MC sample. To take into account the possible difference between MC and data descriptions of splitoff showers, the signal $E_{\text{ECL}}$ shape is calibrated using double tagged events, in which the $B_{\text{tag}}$ is reconstructed in a semileptonic decay as described above and $B_{\text{sig}}$ is reconstructed in the decay chain, $B^- \rightarrow D^{*-0}\ell^-\nu$ ($D^{*-0} \rightarrow D^0\pi^0$), followed by $D^0 \rightarrow K^-\pi^+$. Figure 2 shows the $E_{\text{ECL}}$ distribution in the double tagged sample for data and for the MC simulation scaled to the same luminosity. The background in this control sample is negligibly small. We find the $E_{\text{ECL}}$ distribution of data tends to have a slightly smaller width than MC. The difference between the data and MC is parameterized as a first-order polynomial function of $E_{\text{ECL}}$ obtained by fitting the ratio of data to MC for the $E_{\text{ECL}}$ histograms of the double tagged sample. The ratio and the fit result are also shown in Fig. 2. The $E_{\text{ECL}}$ histogram obtained from the signal MC sample is multiplied by this correction function.

In the final fit, four parameters are allowed to vary: the total signal yield and the sum of $B\bar{B}$ and continuum backgrounds for each $\tau$ decay mode. The ratio of the $B\bar{B}$ to the continuum background is fixed to the value obtained from MC with the normalization correction applied. Other background contributions are fixed to the MC expectation. We combine $\tau$ decay modes by constraining the ratios of the signal yields to the ratio of the reconstruction efficiencies obtained from MC including the branching fractions of $\tau$ decays [10]. Figure 3 shows the $E_{\text{ECL}}$ distribution overlaid with the fit results. The $E_{\text{ECL}}$ distribution for each $\tau$ decay mode is also shown. We see a clear excess of signal events in the region near zero and obtain a signal yield of $n_s = 143^{+36}_{-35}$. The branching fraction is calculated as $B = n_s/(2\varepsilon N_{B^+B^-})$, where $\varepsilon$ is the reconstruction efficiency including the branching fraction of the $\tau$ decay mode and $N_{B^+B^-}$ is the number of $Y(4S) \rightarrow B^+B^-$ events, assuming $N_{B^+B^-} = N_{B}\tau\bar{\tau}$. Table I lists the signal yields and the branching fractions obtained from separate fits to each $\tau$ decay mode and the fit with all three modes combined. The results of the individual fits are consistent within statistics. The $\chi^2$ of the three results is 2.43 for two degrees of freedom, corresponding to a 30% confidence level.

![Figure 2](image_url)

**FIG. 2:** $E_{\text{ECL}}$ distribution for double semileptonic tagged events. The points with error bars are data and the solid histogram is the MC expectation scaled to the luminosity of the data. The dashed histogram is the MC expectation multiplied by the correction function described in the text. The inset shows the ratio of data to the MC expectation and the correction function.

![Figure 3](image_url)

**FIG. 3:** $E_{\text{ECL}}$ distribution of semileptonic tagged events with the fit result for (a) all $\tau$ decay modes combined, (b) $\tau^- \rightarrow e^-\nu\bar{\nu}$, (c) $\tau^- \rightarrow \mu^-\nu\bar{\nu}$ and (d) $\tau^- \rightarrow \pi^-\nu\bar{\nu}$. The points with error bars are data. The hatched histogram and solid open histogram are the background and the signal contributions, respectively.

Systematic errors for the measured branching fraction are associated with the uncertainties in the signal yield, efficiencies and the number of $B^+B^-$ pairs. Unless explicitly stated otherwise, the systematic errors for each
source are obtained by varying the corresponding parameters individually by their uncertainties, repeating the fit procedure and adding differences from the nominal result in quadrature. The systematic errors for the signal yield arise from the uncertainties in the PDF shapes for the signal and for the background. The uncertainty in the signal shape correction function is estimated by changing the parameters of the correction function by their errors and replacing the function with a second-order polynomial (±2.3%). The systematic error from MC statistics is evaluated by varying the content of each bin in the signal \(E_{\text{ECL}}\) PDF histograms by its statistical uncertainty (±0.9%). The main contributions to the systematic errors for the background PDF shapes are statistical errors in the MC histograms (±8.6%), which is estimated in the same way as the signal PDF MC statistical uncertainty. Other large sources are the uncertainties in the background composition. The errors due to the uncertainties in the branching fractions of \(B\) decay modes that peak near zero \(E_{\text{ECL}}\) such as \(B^- \rightarrow D^0 \ell^- \nu_{\ell}\) with \(D^0 \rightarrow K_S^0 K_L^0\), \(K_L^0 \pi^0\) and \(K^- \ell^+ \nu_{\ell}\), and \(B^0 \rightarrow D^+ \ell^- \nu_{\ell}\) with \(D^+ \rightarrow K^0_S \ell^+ \nu_{\ell}\) are estimated by changing the branching fractions in MC by their errors [10] (±4.5%). For branching fractions of \(D\) decays with a \(K_L^0\), we use the values for the corresponding \(D\) decays with \(K_S^0\)’s. Uncertainties in the background from the possible contribution of rare charmless \(B\) decays such as \(B^- \rightarrow \pi^0 \ell^- \nu_{\ell}\), \(B^- \rightarrow K^- \nu_{\ell}\) and \(\ell^- \nu_{\ell}\), and from \(\tau^+\tau^-\) pair and two photon processes are evaluated by changing the fractions obtained from MC by their experimental errors [10] if available, or by ±50% otherwise (±7.7%). The systematic error due to the uncertainty in the normalization correction factor for the continuum MC is +2.6%−2.5%. The systematic error associated with the reconstruction efficiency of the tag-side \(B\) is evaluated by comparing of the \(B(B^- \rightarrow D^{(s)} \ell^- \nu_{\ell})\) branching fraction measured with the double tagged sample in data to the world average value [10]. We obtain the ratio to be 0.907 ± 0.044 and take the difference from unity plus one \(\sigma\) as the systematic error (13.7%). The systematic errors in the signal-side efficiencies arise from the uncertainty in tracking efficiency (1.0%), particle identification efficiency (1.3%), branching fractions of \(\tau\) decays (0.4%), and MC statistics (0.8%). The systematic error due to the uncertainty in \(N_{B^+B^-}\) is 1.4%. The total fractional systematic uncertainty is +19%−20%, and the branching fraction is

\[
B(B^- \rightarrow \tau^- \nu_{\tau}) = (1.54^{+0.38}_{-0.37}(\text{stat})^{+0.29}_{-0.31}(\text{syst})) \times 10^{-4}.
\]

The significance of the observed signal is evaluated by

\[
\Sigma = \sqrt{-2 \ln \left(\frac{L_0}{L_{\text{max}}} \right)},
\]

where \(L_{\text{max}}\) and \(L_0\) denote the maximum likelihood value and likelihood value obtained assuming zero signal events, respectively. The systematic uncertainty is convolved in the likelihood with a Gaussian distribution having a width corresponding to the systematic error of the signal yield. We find the significance of the signal yield to be 3.6\(\sigma\).

In summary, we have measured the decay \(B^- \rightarrow \tau^- \nu_{\tau}\) with \(B\bar{B}\) events tagged by semileptonic \(B\) decays using a data sample containing \(657 \times 10^6 B\bar{B}\) pairs collected at the \(\Upsilon(4S)\) resonance with the Belle detector at the KEKB asymmetric-energy \(e^+e^-\) collider. We measure the branching fraction to be \((1.54^{+0.38}_{-0.37}(\text{stat})^{+0.29}_{-0.31}(\text{syst})) \times 10^{-4}\), with a significance of 3.6 standard deviations including systematics. This result is consistent with the previous Belle measurement using \(B\bar{B}\) events tagged by hadronic \(B\) decays and is consistent with the results reported by the BaBar collaboration. Using the measured branching fraction and known values of \(G_F\), \(m_B\), \(m_\tau\) and \(\tau_B\) [10], the product of the \(B\) meson decay constant \(f_B\) and the magnitude of the Cabibbo-Kobayashi-Maskawa matrix element \(|V_{ub}|\) is determined to be

\[
f_B|V_{ub}| = (9.3^{+1.2}_{-1.1} \pm 0.9) \times 10^{-4} \text{ GeV}.
\]

Using \(|V_{ub}| = (3.89 \pm 0.44) \times 10^{-3}\) in Ref. [10], \(f_B\) is calculated to be 0.24 ± 0.05 GeV. The measured branching fraction is consistent within errors with the SM expectation from other experimental constraints [8]. The result can be used to extract constraints on new physics models.

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