Breaking Down the Parallel Performance of GROMACS, a High-Performance Molecular Dynamics Software

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Abstract—GROMACS is one of the most widely used HPC software packages using the Molecular Dynamics (MD) simulation technique. In this work, we quantify GROMACS parallel performance using different configurations, HPC systems, and FFT libraries (FFTW, Intel MKL FFT, and FFT PACK). We break down the cost of each GROMACS computational phase and identify non-scalable stages, such as MPI communication during the 3D FFT computation when using a large number of processes. We show that the Particle-Mesh Ewald phase and the 3D FFT calculation significantly impact the GROMACS performance. Finally, we discuss performance opportunities with a particular interest in developing GROMACS for the FFT calculations.

Index Terms—Molecular Dynamics, Particle-Mesh Ewald Calculations, Fast-Fourier Transform

I. INTRODUCTION

Molecular Dynamics (MD) [1] is the use of computer simulations to study the physical system particle dynamics and interactions. Today, this technique is widely used in different scientific domains, such as biochemistry and material science, among many others. In particular, the MD software landscape is dominated by a number of well known HPC codes, including GROMACS [2], NAMD [3], and CHARMM [4].

In this work, we investigate the GROMACS parallel performance. GROMACS originated in the early 1990s at the University of Groningen [5] and has since then been developed and maintained as a community effort. It supports an open-source policy and, among its many strengths, can be executed on a large number of systems, including small (personal) laptops all the way to large high-performance computers (HPC) [6]. Furthermore, GROMACS supports both general-purpose processors (CPUs) as well as Graphics Processing Units (GPUs) [7]. However, despite the continuous improvement in hardware technologies, GROMACS (and other MD frameworks) are still challenged - from the computational point of view - to simulate critical biological processes such as protein folding, conformational transition in bio-molecules (such as R to T transition in Hemoglobin), bacterial and viral infections [8], [9]. These simulations require the usage of supercomputers and accelerators. Needless to say, GROMACS is constantly developed and extended to improve its parallel efficiency as well as algorithmic improvements [10] to facilitate the study of larger and more complex molecular simulations.

This paper seeks to understand the GROMACS parallel performance and identify optimization possibilities. For this reason, we run GROMACS on two state-of-the-art HPC systems, analyze their results, and identify key performance-limiting characteristics. In short, our contributions are:

1) A quantitative and systematic performance evaluation of GROMACS on two HPC systems.
2) We study the impact of different GROMACS phases’ implementations, varying the number of processes. We quantify their different impact on the overall GROMACS performance and analyze their respective performance-degrading contribution. For a different number of processes, we identify various optimization opportunities.
3) We quantify the performance impact of using various FFT libraries.

II. BACKGROUND

MD simulations mimic the dynamics of molecules by solving numerically the equation of motion of particles, using for instance Verlet or leap-frog algorithms. To determine the new position and velocities for each particle, we need to calculate the force acting for each particle. Examples of such forces are the van der Walls and the Coulombic forces. While the cost of particle position and velocity calculations scale with the number of particle under study, a naı¯ve algorithm for the calculation of the forces requires to calculate the contribution to the force for each pair of particle present in the system, making the computation scaling as the square of number of particles present in the system.

To decrease the computational complexity of force calculations, modern MD algorithms divide the interactions between the molecules into short-range interaction, such the ones from van der Waals interactions, and long-range interactions, such as electrostatic interactions. For instance, van der Waals forces are short-range in nature and decays with distance rapidly. Short-range interactions are only computed for the neighboring particles within a cut-off distance, usually set to 15-20 Å for
many applications. The force contribution from particles farther than the cut-off distance is neglected, effectively reducing the interaction of one particle to the closest particles only. However, the electrostatic interactions are long-range in nature and farther particles contribute to the its calculations, still requiring \(O(N^2)\) calculations. To solve, this problem, modern MD codes, such as GROMACS, use the PME method.

### A. Particle-Mesh Ewald Computations

The basic (and here simplified for sake of clarity) strategy of the PME technique is to discretize the simulation domain in a uniform computational grid and calculate the charge density for each grid point, for instance using interpolation functions. After the charge density on the grid points is known, the Poisson Equation \(\nabla^2 \Phi = -\rho/\epsilon_0\) is solved on the grid for the electrostatic potential \(\Phi\) and the electric field (still on the grid points) is calculated from it as \(E = -\nabla \Phi\). The electric field information on the grid is transferred to the particle by using again interpolation functions. The PME method use FFT to solve the Poisson equation for electrostatic potential on the grid: we transform first the charge density information to the spectral space, we solve the Poisson equation in the spectral space as algebraic equation (multiplication in spectral space) and then apply an inverse FFT to calculate the potential in the real-space. By working in the spectral spaces, the PME method accounts also for force contributions arising from periodic infinite systems, such as the typical systems studied with MD. In the PME method, 1D FFT (and the inverse 1D FFT) requires \(O(N_g \log N_g)\), where \(N_g\) is the number of grid points. To calculate the electrostatic potential we use first a 3D FFT on a real data input (the charge density), and after the convolution we apply a 3D FFT to move the potential to the physical space. The way to perform a 3D FFT is by using several 1D FFT and transposing the results. In a parallel setup, the transpose operation requires a large number of messages that is the all-to-all communication that scales linearly with the number of processes. Therefore, the all-to-all communication is a potential performance bottleneck [10].

### III. BACKGROUND

MD simulations mimic the dynamics of molecules by numerically solving the equation of particles’ motion using Verlet or leap-frog algorithms. To determine each particle’s new position and velocities, we need to calculate the force acting on each particle. Examples of such forces are the van der Walls and the Coulombic forces. While the cost of particle position and velocity calculations scale with the number of particles under study, a naïve algorithm for the calculation of the forces requires calculating the contribution to the force for each pair of particles present in the system, making the computation scaling as the square of the number of particles present in the system. To decrease the computational complexity of force calculations, modern MD algorithms divide the interactions between the molecules into short-range interactions, such as the ones from van der Waals interactions, and long-range interactions, such as electrostatic interactions. For instance, van der Waals forces are short-range in nature and decay with distance rapidly. Short-range interactions are only computed for the neighboring particles within a cut-off distance, usually 15-20 Å for many applications. The force contribution from particles farther than the cut-off distance is neglected, effectively reducing the interaction of one particle to the closest particles only. However, the electrostatic interactions are long-range in nature, and farther particles contribute to its calculations, still requiring \(O(N^2)\) calculations.

Modern MD codes, such as GROMACS, use the Particle-Mesh Ewald (PME) method to solve this problem. The basic strategy of the PME technique is to discretize the simulation domain in a uniform computational grid and calculate the charge density for each grid point, for instance, using interpolation functions. After the charge density on the grid points is known, the Poisson Equation \(\nabla^2 \Phi = -\rho/\epsilon_0\) is solved on the grid for the electrostatic potential \(\Phi\) and the electric field (still on the grid points) is calculated from it as \(E = -\nabla \Phi\). The electric field information on the grid is transferred to the particle by using again interpolation functions. The PME method use FFT to solve the Poisson equation for electrostatic potential on the grid: we transform first the charge density information to the spectral space, we solve the Poisson equation in the spectral space as algebraic equation (multiplication in spectral space), and then apply an inverse FFT to calculate the potential in the real-space. The PME method also accounts for force contributions arising from periodic infinite systems, such as the typical systems studied with MD, by working in the spectral spaces. In the PME method, 1D FFT (and the inverse 1D FFT) requires \(O(N_g \log N_g)\), where \(N_g\) is the number of grid points. We first use a 3D FFT on a real data input (the charge density) to calculate the electrostatic potential. After the convolution, we apply a 3D FFT to move the potential to the physical space.

GROMACS divides the calculations at different parallelization levels, ranging from MPI to OpenMP, CUDA, and CPU vector instructions. At a high level, GROMACS uses a pipelined parallelism with two main phases: the Particle-Particle (PM) and PME calculations. GROMACS allows dividing the MPI processes into PME processes dedicated only to PME and PP phase responsible for all the other calculations, such as computing the particle dynamics and short-range interactions. The two phases can run in parallel and typically on different kinds of resources, such as different nodes, cores, or devices. To finish a GROMACS computational cycle, the PME phase needs to be completed. This synchronization might introduce a delay in the simulation (causing an idle time on the PP processes) and load imbalance if the PP and PME phases are not finishing at the same time. Naturally, the number of PP and PME MPI processes impacts the load balance and the performance. In GROMACS, the choice of the number of processes dedicated to PME and PP calculations can be set by using the command line (via \(-n\text{pme}\) option) or can be set by GROMACS in preparation for a simulation by an auto-tuning tool: \text{gmx tune_pme} (which is not to be confused with the PME tuning done at run-time). GROMACS allocates
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the simulation and represents the total GROMACS throughput. Each simulation is performed ten times on Beskow and five times on Tetralith, showing a high standard deviation. The figures consist of the mean (median) of these simulations. The simulation parameters are: -notunepme -dlb no and for the GPU -notunepme -dlb no -nb gpu -update -gpu.

Furthermore, to minimize the effects of congestion and impact from the network topology (explained in detail in [17]), every job evaluates all FFT libraries with the same node configuration. This is not done for the Tetralith simulations. On both Beskow and Tetralith, we run with two OpenMP threads per MPI rank, and on Beskow, hyperthreading is turned on by default.

VI. RESULTS

As the first step of our study, we analyze the GROMACS parallel performance. Fig. 1 shows a tracing of a GROMACS run instrumented with Score-P [18] and visualized with the Vampir tool [19]. In this run, four processes (with thread numbers 5, 11, and 17) are dedicated to the PME calculations, while there are 20 PP processes. Within the PME processes, the all-to-all communication is reduced to only four processes decreasing the communication cost for the transposition in the 3D FFT. It is important to note that the PP processes wait for the PME processes to finish in this run, and the PME calculations dominate the computational time step. We can also observe that the PME ranks are severely imbalanced as the 1D FFT calculations (blue) in rank 17 is much slower than the corresponding calculations in rank 5 and 11.

We investigate the total impact of PME calculations on the GROMACS’ total execution time. Fig. 2 shows the fraction of simulation time spent in the PME calculations with respect to the PP time and the total time, varying the total number of cores per GROMACS simulation.

The left panel presents the strong scaling results for the Lysozyme simulations (small-size problem). In this case, the simulation scales up to 256 cores then we observe an increase in the simulation time for 512 cores. In this case, more than 90% of the simulation is spent on MPI communication. We note that the switch from a PP-dominated to PME-dominated simulations appears around 128 cores. In fact, PP scales well beyond 512 cores. There is a significant imbalance between PP and PME. This imbalance can be seen by inspecting the difference between the slowest PP and PME and the total time. The right panel of Fig. 2 presents the results for the Spike strong scaling test. In this case, we observe strong scaling up to 2,048 cores. The simulation is bound by PP up to 256 cores and limited by PME beyond that. We note that PP keeps scaling like in the Lyso case.

After identifying PME as the main obstacle to strong scalability, we analyze which parts of the PME calculations show performance bottleneck and are amenable to performance optimization. Fig. 3 presents a breakdown of the different phases during the PME calculations on the Beskow system with FFTW (the right panel shows the percentage to ease the comparison).

From an analysis of the plots, we note that when a small number of cores are dedicated to PME calculation, the PME spread and gather operations accounts for most of the time. On the contrary, for a larger number of cores, e.g., more than 256 PME cores, the communication for the 3D FFT (parallel transpose) and PME redistribution time dominate the PME calculation and, therefore, the whole simulation time. These two PME phases are responsible for losing scalability at large numbers of the core. Spread and Gather also level out at high core counts but at a lower total cost. At peak performance of the PME calculation, 50% of the time is spent on 3D FFT calculation, and most of that is communication.

An interesting question for GROMACS users is what performance improvement can be achieved by changing the FFT library and what is the best performing one in GROMACS. We compare the results for three PME phases (3D-FFT communication, PME 3D-FFT, and PME redistribution X/F) for different 1D FFT libraries. The results are shown in Fig. 4.

As expected, we do not observe any significant performance change in the communication cost as GROMACS handles the communication, and it remains the same regardless of the library in use. Yet, we notice a difference in individual FFT performance. While for a small number of core counts, FFTW and MKL perform equally well, for a more significant number of cores, the FFT, built with GNU compilers, provides the best performance on Beskow. We also notice that the 3D FFT communication and redistribution measurements are noisy. We also note that the different clusters perform significantly differently: the Tetralith results communication results show a significant performance variability in Fig. 4. We also note that MKL is slightly faster than FFTW.

We present the strong scaling behavior of the interpolation steps in Fig. 5. We notice that the scaling stops at approximately 512 cores for these parts, similar to the FFT communication and redistribution. However, it only displays a reduced performance variability after scaling breaks down compared with the parallel transpose and redistribution. We note that the gather and spread phases make up only 20% of the total PME calculation after they have stopped scaling.

The total performance of the PME calculations, varying FFT libraries, can be seen in Fig. 6. It shows the diminishing effects of the 1D FFT compute and the increasing performance variability coming from the communication with an increased number of cores. It is clear that FFTW and MKL are better choices than FFTPACK and are always motivated choices.

Finally, we analyze the performance of GROMACS PME on GPUs and present the results in Fig. 7. The GPU performance for the Lysozyme test case out-perform the CPU configurations significantly: PME on GPU and bonded calculations on CPU resulted in a throughput of approximately 640 ns/day compared with close to 380 ns/day for 128 CPU cores with FFTW.

We observe a slight advantage in using FFTW as the FFT library with a total throughput increase of 10% compared
Fig. 1. Tracing of a GROMACS run with 24 processes using ScoreP and Vampir tools. Four processes (three visible) complete the PME calculations in this run, while twenty processes quickly carry out the PP calculations. The PP processes wait for the PME processes to finish. We can also see a significant load imbalance between the PME ranks. The dark red is MPI_Alltoall for FFT communication. All other MPI calls are light red. The green color represents the general compute, dark green is gather, blue is 1D FFT, purple is spread, and turquoise is the convolution calculation.

Fig. 2. The fraction of time for PME, PP, and execution time on the Beskow system varying the total number of cores, to the left the Lysozyme system and to the right the Spike system. 1/4 of the cores are dedicated to the PME calculations. In this case, we use FFTW as the FFT library. Due to a lack of complete overlap and synchronization costs, the total execution is longer than each component phase duration.

with the other libraries for the small Lysozyme system. In the Spike test case, GROMACS runs on the Nvidia A100 perform comparably to 512 CPU cores on Beskow (46 ns/day) and a bit better than 512 cores on Tetralith (36 ns/day).

VII. DISCUSSION AND CONCLUSION

In this paper, we presented an evaluation of GROMACS parallel performance. We conclude that the performance of PME is highly correlated with the parallel transpose and the redist functions. Redist is dependent on the domain decomposition of the PP part of the simulation, and therefore their performance is problem specific. The 3D FFT size can be varied to more
accurately solve the Electrostatics or to balance the load. These two are also the parts of the PME calculation with the most variance between runs. We identified three main factors in the GROMACS PME that can be improved. Firstly, there are many classes of problems, such as embarrassingly parallel ensemble jobs or parameter searching jobs, where many simulations can be distributed on many nodes with one job running on a single node. Improving 1D FFT performance for a single node can make noticeable overall performance in such ensemble simulations. Using FFTW or MKL instead of the backup library is advised; FFTW performs twice that of PACK in the spike problem. For the future, a possible further optimization technique is to use batched 1D FFTs parallelized with SIMD vector instructions. Secondly, within the most scalable range,
we can see that the cost associated with the interpolation steps and the transpose are similar in size. We would suggest an overlap between the communication needed from Spread-Gather and the parallel transpose. Since the GROMACS CPU code does not depend on an external 3D FFT library, it might be possible to incorporate the interpolation steps and therefore limit the need for communication. Finally, we have the transpose-dominated range – the Achilles’ heel of the method.

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