Conductance switching and inhomogeneous field melting in the charge ordered manganites

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Abstract – The field-induced switching of conductance in the charge ordered half-doped manganites is controlled by the combination of metastability, an inhomogeneous high-field state, and cation disorder. We study this non-equilibrium problem via real space Monte Carlo on a disordered strong coupling model appropriate to the manganites. We reproduce the variation of the switching fields with the mean ionic radius \( r_A \) and cation disorder \( \sigma_A \), and demonstrate how the experimental features arise from the proximity of several phases in the Landau free-energy landscape. Our prediction for the field melted state is consistent with a growing body of experimental evidence.

The manganites owe their fame to the “colossal magnetoresistance” effect, whereby an applied magnetic field strongly suppresses the resist ance of the material. The most extreme version of this happens when the field can actually induce an insulator-metal transition (IMT). This occurs in the low-bandwidth half-doped manganites, e.g., \( \text{Pr}_{0.5}\text{Ca}_{0.5}\text{MnO}_3 \), that are typically charge-ordered (CO) insulators with CE magnetic order [1–3]. The CE-CO-I state is transformed to a ferromagnetic metal (FM-M) by an applied field through a first-order phase transition. The magnetic-field–induced conversion of the CE order to FM, and the crucial resistive switching, involve several subtleties that are only gradually being appreciated [4–14]. These include the surprising difference between the melting fields in two lanthanide (Ln) families, namely the Ca [4] and the Sr [5,6] families; the smallness of the field melting energy scales [4–7]; and the spatial character of field-induced melting and its relation to structural disorder [8–12]. We expand on these issues below.

i) The phase boundary between the CE and FM phase is first order, so metastable states exist on either side. This leads to hysteresis, and the switching fields are decided by \textit{non-equilibrium effects}, and not by free-energy balance. ii) While trapping into metastable states is expected in a first-order transition, an applied field leads to \textit{new equilibrium states} that are not simple continuation of the zero-field state. In particular, it is increasingly apparent that the field-induced conducting state is an \textit{inhomogeneous} FM-M, a percolative metal with a finite volume fraction of CO regions [8–12]. Finally, iii) the field-induced switching and inhomogeneous metallicity play out on a structurally disordered background. One expects the CO-I state to be more stable in narrow band systems. While this is true in the Ca-based manganites [4], where the cation size mismatch \( \sigma_A \) is small, it is completely opposite in the Sr-based systems [5,6]. The more insulating system can be driven metallic more easily in the presence of disorder!

These three actors, metastability, field-induced inhomogeneity, and pinning disorder, enrich and complicate the field melting problem. There is no understanding of their interplay in the field-induced IMT, and the non-equilibrium physics of the manganites.

We study a coupled electron-spin-lattice model [15] appropriate to the manganites, in two dimensions (2D). For parameters where the FM-M and CE-CO-I phases are in proximity, we discover the following. i) In the “clean” limit, the forward (CE to FM) and reverse (FM to CE) switching fields, \( h^+_c \) and \( h^-_c \), respectively, increase rapidly with decreasing bandwidth (BW), and below a threshold BW the field cannot melt the CO. This explains the results in the “clean” Ca-based manganites. ii) The

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switching fields are dramatically affected by disorder: \( h^\pm \rightarrow 0 \) as the bandwidth reduces, as in the \( 5r \) manganites, even though the CO is notionally stronger. i) The field melted state in the narrow band case is inhomogeneous even without disorder — at finite field the system exists as a patchwork of metallic and CO regions, and the “metallicity” is of percolative origin. Recent experiments have indeed verified the coexistence of FM-M and CO-I, e.g., in \( \text{La}_{0.5}\text{Ca}_{0.5}\text{MnO}_3 \) [11] and \( \text{Pr}_{0.5}\text{Sr}_{0.5}\text{MnO}_3 \) [9,10], and the phase volumes are tunable depending on the field cooling protocol.

We consider the field response of a model \( H_0 \) that we had studied earlier [15] to capture phase competition. Our model is

\[
H = H_0 - \mu \hat{N} + \sum_i \epsilon_i n_i - J \sum_{i<j} S_i \cdot S_j - \lambda \sum_{i<j} Q_i \cdot \tau_i + K \sum_{i<j} Q_i^2
\]

(1)

\( H_0 \) involves two \( \epsilon \) levels per Mn, with nearest neighbour hopping \( t_{\alpha \beta} \) (see footnote 1), and Hunds coupling \( J \) between the \( \epsilon \) electrons and the \( t_{\alpha \beta} \) derived core spins. We assume a 2D square lattice. The \( \epsilon \) electrons have a coupling \( \lambda \) to Jahn-Teller phonons, while the core spins have an anti-ferromagnetic (AF) superexchange \( J \) between them. The stiffness of the phonon modes is \( K, \mu \) is the chemical potential, and the magnetic field, \( \hat{h} = \hat{z} h \), couples to the core spins. The “phonons” are treated in the adiabatic limit and provide a static distortion background for the electrons. The core spins are also treated as classical [16]. At half-doping, \( n = 0.5 \), the clean model has a variety of phases of which we are interested in the CE-CO-I phase and its response to a magnetic field. Cation disorder leads to “site disorder” due to the potential generated by the randomly located rare earth and alkaline earth ions, and “bond disorder” in \( t_{ij} \) and \( J \). We retain only the local random potential since it couples to the electron density and has a direct impact on order charge. It was recently shown [17] that while off-diagonal disorder is crucial for obtaining the spin glass phases at half-doping, it is diagonal disorder that plays a dominant role in weakening and eventual disruption of the CO state. We model the potential \( \epsilon_i \) seen at the Mn site as binary distribution \( P(\epsilon_i) = 1/2(\delta(\epsilon_i - \Delta) + \delta(\epsilon_i + \Delta)) \) with variance \( \Delta^2 \). For \( H_0 \), we use \( JH/t \to \infty \) and set \( |S_i| = 1 \).

We use the travelling cluster approximation (TCA) based Monte Carlo method [18] to solve the coupled electron-spin-phonon system above. Classical Monte Carlo techniques have been extensively used in the literature [19] to study first-order transitions and the associated hysteresis. We will explore the dependence of the melting process on bandwidth (\( \lambda/t \)), disorder (\( \Delta/t \)) and temperature \( T/t \). The experimental variation of bandwidth (via \( r_A \)) implies simultaneous change in \( \lambda/t, J/t, \) and \( T/t \), while we have varied \( \lambda/t, J/t \) and \( \Delta/t \) independently. Our primary variation is in \( \lambda/t \) and, crudely, we compare this to experimental BW variation. We have commented on this in more detail elsewhere [20]. All our results are for cooling at \( h = 0 \) followed by field sweep. The “upper” and “lower” switching fields, \( h^\pm \), in the hysteretic response refer to the resistive transitions.

The field-induced melting of CO has been studied within mean-field theory (MFT) earlier. For a model involving double exchange and Coulomb effects Mishra et al. [21] showed that suitable parameter choice could lead to a low \( h_c \sim 6T \). Fratini et al. [22] considered a more elaborate model and worked out typical \( h-T \) phase diagrams within MFT, and Cepas et al. [23] used a variational approach at \( T = 0 \) to estimate \( h_c \). These studies, unfortunately, do not shed light on the spatial character of melting or the impact of disorder.

Let us first clarify the field melting and hysteresis in manganites with weak cation disorder. \( \sigma_A \) is small, \( \sim 10^{-3}A^2 \), in the lanthanide (La) family \( \text{Lu}_{0.5}\text{Ca}_{0.5}\text{MnO}_3 \) [4] so as reference we look at \( \text{La}_{0.5}\text{Ca}_{0.5}\text{MnO}_3 \) (LCO), with a relatively large BW,
and Pr$_{0.5}$Ca$_{0.5}$MnO$_3$ (PCMO), with a smaller BW. Figures 1(a) and (b) reproduce the $h-T$ phase diagrams for these compounds from [4]. At low temperature, $h^c_-$ is $\sim 20\,T$ for LCMO and $\sim 30\,T$ for PCMO. The field $h^c_-$ at which CO is recovered on field reduction is, however, $< 1\,T$ in LCMO but $\sim 15\,T$ in PCMO. $h^c_- \sim 0$ at low temperature in LCMO indicates that the FM-M is metastable even at $h = 0$, while at smaller BW (PCMO) the FM-M is no longer metastable at $h = 0$. The $T_{CO}$ at $h = 0$ for these two systems are $\sim 220$ and $250\,K$, respectively.

Panels (c) and (d) show $h-T$ phase diagrams computed by us at two couplings. For the lower value, $\lambda/t = 1.55$, $T_{CO}/t \sim 0.05$, while for $\lambda/t = 1.60$, $T_{CO}/t \sim 0.06$. Using a crude factor of $3/2$ to convert from 2D to 3D and setting $t \sim 0.25\,eV$, these would correspond to about $210\,K$ and $250\,K$. More significantly, $\lambda/t = 1.55$, which is closer to the (FM-M CO-I) phase boundary, shows $h^c_- = 0$, akin to LCMO, while at $\lambda/t = 1.6$, $h^c_-$ is finite and the FM-M state is no longer metastable at $h = 0$. Although our $h^c_-$ scales, $\sim 0.1t$, are larger than in experiments$^2$, the typical value $\frac{1}{2}(h^c_+ + h^c_-)$ varies roughly similarly in the experiments and theory, changing from $10\,T$ to $20\,T$ between LCMO and PCMO and $\sim 0.05t$ and $0.08t$ in fig. 1(c) and (d). It is possible that including electron-electron interaction may reduce the melting fields somewhat [22] as mean-field studies suggest. The $h-T$ phase diagram is derived from the evolution of the $q = \{0,0\}$ feature in the magnetic structure factor $S(q)$ and the “volume fraction” $V_{CO}$ (see footnote $^3$) of the CO phase.

Figure 2 shows these features at $\lambda/t = 1.6$ and $T/t = 0.02$. Figure 2(a) shows the “switching” of $V_{CO}$ and $S_{fm} = S(0,0)$ on field cycling, for a clean system. The complementary switching in FM and CO volume fraction is sharp and simultaneous, along with the transition in resistivity $\rho(h)$ shown in fig. 2(b). Notice the residual $V_{CO}$ in the field melted metallic state in fig. 2(a). For a weakly disordered CO state, at $\Delta/t = 0.12$, fig. 2(c) shows that the CO melts on increasing $h$, but fails to recover on downward sweep. The magnetism in fig. 2(c) and $\rho(h)$ in fig. 2(d) still show hysteresis but the transitions are quite broad. This suggests that the field-induced “melting” in the disordered case occurs gradually, unlike the abrupt switching in the clean case.

Using indicators as shown in figs. 1 and 2, we made a comprehensive comparison between experiment and theory for the dependence of transition temperatures

$^2$This smallness of $h_c$ is due to the proximity of the FM-M and CE-CO-I phases over a large part of parameter space in 3D. Within our 2D framework, the FM-M and CE-CO-I neighbour each other only over a narrow window, and are otherwise separated by a magnetic phase (“A-2D”) with ordering at $q = \{0,\pi\}, \{\pi,0\}$. This increases $\mathcal{E}_{FM} - \mathcal{E}_{CO}$ and, thus, the $h_c$. Since we have not fine-tuned parameters so that $\mathcal{E}_{FM} \approx \mathcal{E}_{CO}$, our typical $h_c$ are somewhat large.

$^3$Our CO volume fraction is a measure of the local CO correlation, obtained by essentially counting the number of sites on the lattice that are correctly coordinated to form a local $(\pi,\pi)$ charge order. We prefer this “short-range” measure since it is useful in both 2D and 3D, and correlates with the transport. Features depending on long-range order will not survive the effect of disorder in 2D.

Fig. 2: (Colour on-line) Response to field cycling at $\lambda/t = 1.6$ and $T/t = 0.02$. (a), (b) Clean system $\Delta/t = 0$: (a) field response of the CO volume fraction (see text) and the FM structure factor $S_{fm}$; (b) the resistivity $\rho(h)$; (c), (d) corresponding results in the disordered case $\Delta/t = 0.12$. Shaded region is the hysteretic window. Contrast the abrupt switching in the clean limit with the broad crossover in the disordered case. Note, both the CO volume fraction and the FM magnetic structure factors are normalised to unity.
correct dependence. The fall in $T_{CO}$ at large $\lambda/t$ is due to the competition between the “stiffness” $(K_{eff}(\lambda))$, say of the CO state, which weakens at large $\lambda/t$ [24], and the pinning effect of the random potential $\epsilon_i$. This is similar to the random field Ising model [25] where the exchange $(J_{eff})$ serves the role of our “stiffness” and the random field $(h_i)$ is akin to $\epsilon_i$. As is well known, long-range order is lost below a threshold for $J_{eff}/\sqrt{(h_i^2)}$, equivalent to our $K_{eff}/\Delta$. The weakening and ultimate destruction of the zero-field CO state with decreasing $r_A$ (or $t/\lambda$) automatically suppresses the melting fields $h^*_c$. The non-monotonic character of $T_{CO}$ and $h_c$, with a reduction also at the large BW end, is due to the presence of the competing FM-M phase at $\lambda/t < 1.5$.

While the trends are well captured, let us compare the experimental $T_{CO}$ scales with theory. At the “large” BW end, $r_A \sim 1.36 \AA$, “clean” LCMO has $T_{CO} \sim 220\text{K}$, while “disordered” $Pr_{0.5}Sr_{0.5}MnO_3$ (PSMO) has a suppressed $T_{CO} \sim 150\text{K}$. If we identify $\lambda/t \sim 1.55$ crudely as the equivalent, the clean $T_{CO}$ is $\sim 0.055t \sim 225\text{K}$, and the “disordered” $T_{CO}$ is $\sim 0.035t \sim 145\text{K}$. The peak $T_{CO}$ is $\sim 160\text{K}$ in fig. 3(b) and it is $\sim 0.05t \sim 200\text{K}$ in theory. Given that we are solving a 2D model and have not fine-tuned parameters, the correspondence is reasonable.

The thermodynamic indicators, however, do not reveal the spatial character of the “melted” state, while figs. 2(a) and (c) suggest something unusual: there is finite CO phase fraction in the “FM-M”! Our map of the density field in fig. 4 reveals how the system is spatially organised. The lower panels show that the CE phase transforms to an FM at large field (and only partially recovers CE order on reverse sweep), but the large $h$ density field is strongly inhomogeneous. The middle panel, top row, shows charge modulated “minority” regions in a homogeneous background, surviving way past the CE$\rightarrow$FM transition. For the parameter values in fig. 4, and overall for $\lambda/t < 1.6$, the “high-field” state is a percolative metal. Beyond $\lambda/t = 1.6$, it is an insulating FM-CO.

Fig. 4: (Colour on-line) Spatial snapshots of local charge order (top row) and the nearest neighbour magnetic correlation $S_i\cdot S_j$ (bottom row) on field cycling, $\lambda/t = 1.55$, $\Delta/t = 0$ and $T/t = 0.02$; $h = 0$ (left) initial state, $h > h^*_c$ (centre), and $h = 0$ (right) after the field sweep. The lattice size is $40 \times 40$. In the bottom panel the red bonds are FM, the green bonds are AF.

In the top panel grey regions imply metallic regions and the red and green regions are the $0.5 - \delta$ and $0.5 + \delta$ on-site charge densities.

Fig. 5: (Colour on-line) Landau landscape. We plot the free energy $F(\phi,h)$, where $\phi$ is the “order parameter” (on the $x$-axis) and can have FM-M, CE-CO-I, AF-M or AF-CO character. $h$ increases from $h_1$ to $h_3$ (on the $y$-axis). We have not shown the metastable FM-CO state, for $h \sim h_2$, to avoid cluttering.

Fig. 3: (Colour on-line) $T_{CO}$ and $h^*_c$ at low $T$ — comparing experiment and theory. (a), (b) Data from experiments: (a) the $La_{0.5}Ca_{0.5}MnO_3$ family, with typical $\sigma_A \sim 10^{-2} \Omega^{-1}\text{cm}^{-1}$, and (b) the $La_0.5Sr_0.5MnO_3$ family with typical $\sigma_A \sim 10^{-3} \Omega^{-1}\text{cm}^{-1}$. Notice the rapid increase in $h^*_c$ with decreasing $r_A$, and the collapse of $h^*_c$ with decreasing $r_A$. The weakening and ultimate destruction of the CO state, which is lost below a threshold for $\lambda/t < 1.0$.
The peculiar high-field state requires us to examine the various phases that “compete” in the manganites around \( x \sim 0.5 \) at finite \( h \). At \( h = 0 \) the \( x = 0.5 \) CE-CO-I is separated from an FM-M phase at lower \( x \), and an AF-M phase at larger \( x \), by windows of PS [15]. However, beyond a small threshold field a homogeneous \( x = 0.5 \) state is no longer possible [20] and the \( x = 0.5 \) system breaks up into either (a) \( x < 0.5 \) FM-M and \( x > 0.5 \) AF-M patches, for \( \lambda/t < 1.6 \), or (b) \( x < 0.5 \) FM-CO and \( x > 0.5 \) AF-M patches for \( \lambda/t > 1.6 \). These intermediate field states evolve, respectively, into a homogeneous FM-M or FM-CO state at large \( h \). While the finite equilibrium state is complicated by PS, fieldsweep experiments (and our simulation) also probe the existence of metastable states in which the system can get trapped. Figure 5 summarises the situation at \( h > 0 \), the CE-CO-I is the absolute minimum while the FM-M is metastable (see fig. 1(c)). This continues to finite \( h \), we show a typical field \( h = h_1 \). At \( h = h_2(\lambda) \), the \( x = 0.5 \) state phase separates into AF-M and FM-M, and there is also a metastable FM-CO. Finally, at some \( h = h_3(\lambda) \) the equilibrium state is a homogeneous FM-M but the continuing presence of the low-energy metastable FM-CO state would affect all low \( T \) field sweep experiments.

To conclude, we have clarified how non-equilibrium effects and disorder control the field-driven conductance switching and insulator-metal transition in the half-doped manganites. We discover that the field-induced conducting state is spatially inhomogeneous, even in the absence of quenched disorder. Our results on the \( h-T \) phase diagram and the spatial character of the melted state address existing results and a growing body of spatially resolved data.

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