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Splitting between Bright and Dark excitons in Transition Metal Dichalcogenide Monolayers

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The optical properties of transition metal dichalcogenide monolayers such as the two-dimensional semiconductors MoS$_2$ and WSe$_2$ are dominated by excitons, Coulomb bound electron-hole pairs. The light emission yield depends on whether the electron-hole transitions are optically allowed (bright) or forbidden (dark). By solving the Bethe Salpeter Equation on top of GW wave functions in density functional theory calculations, we determine the sign and amplitude of the splitting between bright and dark exciton states. We evaluate the influence of the spin-orbit coupling on the optical spectra and clearly demonstrate the strong impact of the intra-valley Coulomb exchange term on the dark-bright exciton fine structure splitting.

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Introduction.— Transition metal dichalcogenide (TMDC) monolayers (MLs), with chemical formula MX$_2$, with M=Mo or W and X=S, Se or Te, are semiconductors with a direct bandgap in the visible region situated at the K-point of the Brillouin zone [1, 2]. In these 2D systems the broken inversion symmetry of the crystal lattice allows for optical control of the valley degree of freedom [3–6]. Combined with strong spin-orbit coupling (SOC) this leads to valley-spin locking [7], opening exciting avenues for original applications in optoelectronics and spintronics. Tightly bound excitons [8–11], with binding energies around 0.5 eV, originate from the direct term of the electron-hole (e-h) Coulomb interaction, enhanced by the strong 2D quantum confinement, the large effective masses, and the reduced dielectric screening in 2D systems. While the energy spectra of these excitons have been intensively studied by combining both experimental and theoretical technics in the last years [12–17], little is known about their fine structure.

For optoelectronics based on TMDC MLs it is important to clarify if the lowest energy transition is optically bright or optically dark (i.e. spin forbidden) [18]. This bright-dark exciton fine structure splitting governs the optical properties also of 2D semiconductor nanostructures such as III-V and II-VI quantum wells [19–23] as well as CdSe nanocrystals [24]. In particular, the measured low photo- or electro-luminescence yield and its increase with the temperature in monolayer WSe$_2$ has been interpreted recently in terms of dark excitons lying at lower energy compared to the bright ones [25–29]. This will also affect the efficiency of recently demonstrated WSe$_2$ or WS$_2$ light emitting devices [30, 31]. For fundamental physics experiments an optically dark ground state can be an advantage, as it allows to study exciton quantum fluids in Bose-Einstein condensates [32]. It is thus crucial to determine both the amplitude and sign of this bright-dark exciton splitting in TMDC MLs.

Figure 1b) presents the schematics of a typical TMDC ML band structure in a single particle picture. In addition to the large spin-orbit splitting $\Delta_v$ between A and B valence bands (VBs), the interplay between inversion asymmetry and spin-orbit interaction also yields a smaller spin-splitting ($\Delta_c$) between the lowest energy conduction bands (CBs) [33–36]. First let us consider A-excitons, with the transitions involving only the highest VB energy (A) and the two lowest CBs ($\uparrow\uparrow$ or $\downarrow\downarrow$), see Figure 1a). Here $\Omega_{\uparrow\uparrow}$ represents dark (spin forbidden) transitions, and $\Omega_{\downarrow\downarrow}$ shows bright transitions. As a first approximation, one could consider that the energy splitting $\Delta_{\text{Dark-Bright}} = \Omega_{\uparrow\uparrow} - \Omega_{\downarrow\downarrow}$ between bright and dark excitons is mainly due to the CB splitting $\Delta_c = E_{\text{CB} \downarrow} - E_{\text{CB} \uparrow}$ induced by SOC. Depending on the material, $\Delta_c$ can either be negative for WX$_2$ or positive for MoX$_2$ systems (X=S, Se), as standard functional theory (DFT) and tight-binding calculations have shown [33, 34, 37–40]. However, this single particle approach misses a key ingredient for the accurate determination of the dark-bright exciton splitting: the short-range part of the e-h Coulomb exchange interaction for the exciton [19, 21, 41]. So far in the context of TMDC MLs only the effects of the long-range exciton exchange interaction on the valley dynamics of bright exciton states in TMDC monolayers have been studied [42–45]. Here we demonstrate that the e-h exchange interaction within the exciton causes a splitting between the low energy optically bright and dark excitons in TMDC MLs. We find a giant exchange term of the order of 20 meV, more than 100 times larger than in GaAs quantum wells for instance [19, 21, 41]. For all the investigated MoX$_2$ and WX$_2$ MLs, this local field effect due to the exchange interaction is added algebraically to the CB spin-orbit term $\Delta_c$, yielding a splitting $\Delta_{\text{Dark-Bright}}$ between bright and dark exciton that differs significantly from $\Delta_c$, see comparison in Figure 1a). We find that for MoX$_2$ systems, A-exciton dark states are higher in
energy than bright ones, whereas this order is reversed for WX$_2$ MLs. Interestingly for WSe$_2$ ML we obtain $\Delta_{\text{Dark-Bright}} = -16$ meV, a value in good agreement with a first experimentally derived value [28]. Importantly, we also report results on the exciton states involving the B valence band, which are fully consistent when compared to $\Delta_{\text{Dark-Bright}}$ for the A exciton, since the conduction band splitting contributes with the opposite sign. Moreover we show that the determination of the CB spin-orbit splitting $\Delta_{c}$ requires to perform DFT-based calculations within the GW approach [46, 47]. Significant changes compared to standard DFT level calculations [12, 13, 33, 39] are obtained for all TMDC MLs.

**Computational Details.**— The atomic structures, the quasi-particle band structures and optical spectra are obtained from DFT calculations using the VASP package [48, 49]. Heyd-Scuseria-Ernzerhof (HSE) hybrid functional [50–52] is used as approximation of the exchange-correlation electronic term, as well as the Perdew-Burke-Ernzerhof (PBE) one [53]. It uses the plane-augmented wave scheme [54, 55] to treat core electrons. Fourteen electrons for Mo, W atoms and six for S, Se ones are explicitly included in the valence states. All atoms are allowed to relax with a force convergence criterion below 0.005 eV/Å. After primitive cell relaxation at the PBE level, the optimized lattice parameters, given in Table I are in good agreement (1%) with previous calculations [56] with all values slightly larger than the bulk experimental ones. A grid of 12×12×1 k-points has been used, in conjunction with a vacuum height of 17 Å, to take benefit of error’s cancellation in the band gap estimates [57], and to provide absorption spectra in reasonable agreement with experiments as suggested in different works [58, 59]. A gaussian smearing with a width of 0.05 eV is used for partial occupancies, when a tight electronic minimization tolerance of 10$^{-8}$ eV is set to determine with a good precision the corresponding derivative of the orbitals with respect to $k$ needed in quasi-particle band structure calculations. Spin-orbit coupling was also included non-self-consistently to determine eigenvalues and wave functions as input for the full-frequency-dependent GW calculations [60] performed at the $G_0W_0$ level but also at GW$_0$ level with 3 iterations of the $G$ term, when necessary. The total number of states included in the GW procedure is set to 600, after a careful check of the direct band gap convergence, to be smaller than 0.1 eV. All optical excitonic transitions have been calculated by solving the Bethe-Salpeter Equation as follows [61, 62]:

$$\left(\varepsilon_{v}^{QP} - \varepsilon_{v}^{QP}\right)A_{vc} + \sum_{v'c'}\langle v|e\rangle K^{ch}\langle c'|v'\rangle A_{v'C'} = \Omega A_{vc}, \quad (1)$$

where $\Omega$ are the resulting $e-h$ excitation energies. $A_{vc}$ are the corresponding eigenvectors, when $\varepsilon_{v}^{QP}$ are the single-quasiparticle energies obtained at the $G_0W_0$ level, and $K^{ch}$ being the CB electron-VB hole interaction kernel. This term consists in a first attractive screened direct term and a repulsive exchange part. Practically we have included the six highest valence bands and the eight lowest conduction bands to obtain eigenvalues and oscillator strengths on all systems. Dark excitons are characterized by oscillator strengths around one thousand times smaller than bright ones [63].

**Results and Discussion.**— Figure 1a) and Table I present the calculated values of the splittings $\Delta_{\text{Dark-Bright}}$ between non-optically active 1s exciton transitions $\Omega_{\uparrow\downarrow}$ and active ones $\Omega_{\uparrow\uparrow}$. This splitting is positive for A excitons in the cases of MoSe$_2$ and MoTe$_2$ MLs. These re-
The MoS$_2$ ML is very intriguing, our calculations show that the CB spin-orbit splitting and the exciton exchange term almost cancel each other yielding a very small bright-dark exciton separations. As a consequence, $\Delta_{\text{Dark-Bright}}$ is negative for PBE-based calculations (-5 meV) and 0 meV when HSE orbitals are used. This is in line with the previous determination of Qiu et al [17] for the same system, since $\Omega_{\uparrow\downarrow}$ is lower in energy than $\Omega_{\uparrow\uparrow}$ by approximatively 17 meV and $\Omega_{\downarrow\downarrow}$ by around 23 meV with respect to $\Omega_{\uparrow\downarrow}$. We observe the same trend, the difference being certainly due to our larger $\Delta_c$ values obtained at the GW level, see below. On the B exciton, we also observe a small decrease of the direct contribution that makes the absolute energy difference between the parallel and anti-parallel spins slightly smaller that the simple addition of the conduction band splitting and the exciton exchange term.

| Monolayer | $\Delta_{\text{PBE}}-\Delta_{\text{G}}$ (eV) | $\Delta_{\text{G}}$ | $\Delta_{\text{Dark-Bright}}$ (meV) |
|-----------|---------------------------------|-----------------|-----------------|
| MoS$_2$   | 0.18                            | 0.16            | -24 (-20)       |
| MoSe$_2$  | 0.24                            | 0.22            | 16 (11)         |
| MoTe$_2$  | 0.33                            | 0.26            | 34 (25)         |
| WS$_2$    | 0.45                            | 0.38            | -11             |
| WSe$_2$   | 0.49                            | 0.43            | -16             |

$^a$Reference [64]
$^b$Reference [65]
$^c$Reference [66]
$^d$Reference [67]
$^e$Reference [11]

TABLE I: $\Delta_{\text{PBE}}-\Delta_{\text{G}}$: calculated energy splitting between 1s A and B bright excitons, $\Delta_{\text{Dark-Bright}}$: calculated dark-bright energy separation for various TMDC MLs of the 1s state excitons at the $G_0W_0+BSE$ level using HSE orbitals, the values in parentheses are extracted from $G_0W_0$-PBE calculations.
DFT-based reports [33, 38, 39, 56]. It clearly shows that adding a partial exact exchange contribution to the electronic exchange-correlation functional significantly enlarges $\Delta_e$ for all TMDC MLs. This trend is directly observable in the computed absorption spectra and more specifically in the $\Delta_{B^{-}\rightarrow A^{+}}$ results of Table I which include contributions both from $\Delta_e$ and $\Delta_c$, but also $e\cdot h$ interaction effects. HSE-based calculations always give larger A-B splittings than the experimental estimates, but still remain in a reasonable agreement with them. Considering $\Delta_c$, at the DFT level, our results are similar to previous reports [33, 39]: for the MoX$_2$ family, when going from a semi-local to a hybrid approximation of the electronic exchange-correlation term, the splittings between spin-up and down CB states are enhanced, see Figure 2 and Supplemental Material [68]. Interestingly for the WS$_2$ and WSe$_2$ cases, if now $\downarrow$-CB is the lowest unoccupied state, the energy separation is significantly reduced in hybrid functional calculations, meaning that short-range Hartree-Fock term strongly influence both atomic SOC contributions from the transition metal and from the chalcogen, to make them competitive with opposite signs [33]. For the MoS$_2$ and MoSe$_2$ cases, our $G_0W_0$ calculations based on PBE or HSE wave functions provide similar $\Delta_c$ splittings suggesting a non-dependence band splitting on the ground state orbitals in contrast with MoTe$_2$ ML, probably due to an overestimation of the chalcogen contribution using HSE-based orbitals, which leaves $\Delta_c$ 40% larger even after applying a single shot GW correction. Remarkably for W-based systems the GW scheme reduces drastically $\Delta_c$ starting from PBE orbitals, and even reverses again the spin-up and spin-down conduction bands ordering in HSE-based calculations. This clearly indicates that $\uparrow$ and $\downarrow$ CB states are almost degenerate at the GW level, contrary to standard DFT predictions.

The $G_0W_0$ results reveal further interesting details: as it has been already reported [56] and mentioned in the present letter, all the extracted values of GW calculations, namely $\Delta_c$, $\Delta_e$, and $E_k$ (free carrier gap value) are sensitive to the choice of starting set of orbitals. Larger values of $E_k$ are yielded and a better agreement with previous calculations of the exciton binding energies are obtained when HSE wave functions are used, as shown in the Supplemental Material [68]. Unexpectedly, PBE-based calculations give an indirect band gap in $K_x^-\Lambda$, with values smaller by 0.03 and 0.05 eV respectively when compared to direct $K_x^-K_x$ gaps for WS$_2$ and WSe$_2$. However these surprising results agree with a recent experimental result [70]. The choice of lattice parameter value is also important for the resulting band structure properties: using the experimental lattice parameter results in different values for $\Delta_e$, mainly. Preeminently most of the systems have an indirect band-gap with this particular choice of the lattice parameter [68], even after the use of partially self-consistent $GW_0$ scheme. This conforts us in our particular choices of exchange-correlation functional (HSE) at the DFT level and of the lattice parameter values (optimized ones), for which all MLs have direct band-gaps in good agreement with previous studies.

Conclusions.—Our calculations demonstrate that the bright to dark exciton energy splitting in MoX$_2$ and WX$_2$ monolayers depends in both sign and amplitude on the electron-hole short range Coulomb exchange within the exciton. In addition to this exchange energy, the conduction band spin-orbit splitting $\Delta_s$ needs to be taken into account, which has initially been put forward as the main origin of the dark-bright exciton splitting. To measure the splitting between $\Delta_e$, between electron spin states in the absence of holes, techniques like angle resolved photoemission spectroscopy (ARPES) [71] or electron spin resonance would be desirable, as pure optical spectroscopy techniques (absorption, emission) cannot separate this contribution from the strong electron-hole Coulomb exchange effects.

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[68] See Supplemental Material at url, which includes detailed tables for the valence and conduction band splittings, as well as free carrier band-gaps results and extracted binding energies of the A 1s-states. Dark-bright splittings on B excitons are also depicted and a symmetry analysis of exciton symmetry is presented.
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