Mixing and Shifting: Exploiting Global and Local Dependencies in Vision MLPs

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Abstract

Token-mixing multi-layer perceptron (MLP) models have shown competitive performance in computer vision tasks with a simple architecture and relatively small computational cost. Their success in maintaining computation efficiency is mainly attributed to avoiding the use of self-attention that is often computationally heavy, yet this is at the expense of not being able to mix tokens both globally and locally. In this paper, to exploit both global and local dependencies without self-attention, we present Mix-Shift-MLP (MS-MLP) which makes the size of the local receptive field used for mixing increase in respect to the amount of spatial shifting. In addition to conventional mixing and shifting techniques, MS-MLP mixes both neighboring and distant tokens from fine- to coarse-grained levels and then gathers them via a shifting operation. This directly contributes to the interactions between global and local tokens. Being simple to implement, MS-MLP achieves competitive performance in multiple vision benchmarks. For example, an MS-MLP with 85 million parameters achieves 83.8\% top-1 classification accuracy on ImageNet-1K. Moreover, by combining MS-MLP with state-of-the-art Vision Transformers such as the Swin Transformer, we show MS-MLP achieves further improvements on three different model scales, e.g., by 0.5\% on ImageNet-1K classification with Swin-B. The code is available at: https://github.com/JegZheng/MS-MLP.

1 Introduction

Showing promise in modeling visual dependencies, Vision Transformers (ViTs) have advanced the state of the art (SoTA) of many different visual tasks (Dosovitskiy et al., 2020; Touvron et al., 2020; Liu et al., 2021b). However, the self-attention module (Vaswani et al., 2017), which is key to the ViT success in capturing long-range visual dependencies, involves a computationally intensive operation that compares pairwise similarity between tokens. Inspired by self-attention, but without its heavy computation, several works show that building models solely on multi-layer perceptrons (MLPs) can achieve surprisingly promising results on ImageNet (Deng et al., 2009) classification with both spatial- and channel-wise token mixing (Tolstikhin et al., 2021; Touvron et al., 2021; Liu et al., 2021a). These MLP-based models are efficient in token mixing to aggregate the spatial information and model visual feature dependencies, achieving results competitive to previous models on several representative computer vision tasks, such as image classification, object detection, and semantic segmentation.

Extensive studies of MLPs can be categorized into two mainstream directions depending on whether capturing global or local visual dependencies. Inspired by ViTs, global-mixing MLP-based methods such as MLP-Mixer (Tolstikhin et al., 2021) and ResMLP (Touvron et al., 2021) achieve the global reception field with the communication between patch tokens through spatial-wise projections. In this direction, researchers explore to effectively handle all tokens with various techniques, such as gating, routing, and Fourier transforms (Liu et al., 2021a; Lou et al., 2021; Rao et al., 2021; Tang et al., 2021a;b). Apart from MLPs that explore the modeling of global visual dependencies, a large number of studies have also achieved progress in using MLP-based architectures to model local visual dependencies, as done in the classical convolution paradigm (LeCun et al., 1995). Different from global-mixing architectures, local-mixing MLPs sample nearby tokens for interactions. In this direction several studies achieve effective token sampling by exploiting spatial shifting, permutation,
and pseudo-kernel mixing (Yu et al., 2021; Hou et al., 2021; Mao et al., 2021; Lian et al., 2021; Chen et al., 2021b; Guo et al., 2021), etc.

Despite the success from both perspectives, MLPs still avoid the self-attention at the expense of not being able to mix tokens as flexibly and efficiently as self-attention. The global-mixing is less flexible in identifying the importance among all tokens, while local-mixing is not able to capture long-range dependencies. In this paper, we investigate whether MLPs can effectively capture both short- and long-range dependencies to further improve performance. Intuitively, the visual dependencies between neighboring regions are usually more significant and need more attention, while those far away are still not trivial at a glance. Therefore, we propose to mix tokens from fine- to coarse-levels, where we perform fine-grained mixing in neighboring regions to achieve token interactions locally, while coarse-grained mixing for distant tokens to capture long-range dependencies. Specifically, we propose a multi-scale regional mixing, where the size of the regional receptive field used for mixing is proportional to the relative distance with respect to the query token, and these multi-scale regions are aggregated with a shifting operation. We plug in such multi-scale regional mixing into MLP architecture as Mix-Shift-MLP (MS-MLP). We evaluate the performance of MS-MLP via a comprehensive empirical study on a series of representative computer vision tasks, including image classification, object detection, and segmentation. According to the results, given a similar model complexity, our MS-MLP consistently outperforms SoTA MLPs across various settings, e.g., MS-MLP-B achieves 83.8% in ImageNet-1K classification, which is on par with Focal-Attention-B (Yang et al., 2021) with superior throughputs. In addition, we plug our MS-MLP module into SoTA Transformer models, which further improves both performance and efficiency. Notably, with MS-MLP, Swin Transformers (Liu et al., 2021b) and Focal Transformers (Yang et al., 2021) respectively get improved on average by 0.5-0.6% / 0.2-0.6% in image classification and 0.2-0.5% / 0.1-0.3% in object detection and segmentation.

2 Related works

Global token-mixing MLPs: Global token-mixing MLPs are first proposed as self-attention-free alternatives to Transformer architectures (Tolstikhin et al., 2021; Melas-Kyriazi, 2021; Touvron et al., 2021). MLP-Mixer (Tolstikhin et al., 2021) replaces the self-attention layer of ViT with a spatial-wise MLP projection of tokens, achieving results that are competitive with ViT. gMLP (Liu et al., 2021a), consisting of an MLP-based module with multiplicative gating, provides competitive results in both vision and natural language processing (NLP) tasks. Vision Permutator (Hou et al., 2021) focuses on global mixing along both the vertical and horizontal axes. Raft-MLP (Tatsunami & Taki, 2021) employs a hierarchical and serialized structure which continuously improves accuracy. Similar to the parameterization of query and key pairs in ViTs, Wave-MLP (Tang et al., 2021b) reweighs the importance of tokens with the amplitude and phase modules parameterized by two MLP projections.

Local token-mixing MLPs: Local token-mixing MLPs focus more on the token interactions at local regions and hence share more similarities with convolutional neural networks (CNNs) than with Transformers. They have also been proved to achieve good performance on computer vision tasks. For example, a spatially shifted MLP (S$^2$-MLP) (Yu et al., 2021, 2022) takes spatial shifts in four directions and mixes them in a channel-wise manner to gather information from neighboring tokens. Similar to S$^2$-MLP, an axial-shifted MLP (AS-MLP) (Lian et al., 2021) changes the spatial shifts in both the horizontal and vertical axes to gather local region information. CycleMLP (Chen et al., 2021b) takes pseudo-kernels and sample tokens from different spatial locations for mixing. ConvMLP (Li et al., 2021) incorporates convolution layers and a pyramid structure to achieve local token mixing. Hire-MLP (Guo et al., 2021) rearranges tokens across local regions to gain performance and computational efficiency.

ViTs and CNNs: Transformers (Vaswani et al., 2017), originated from the NLP area, have recently been applied to visual tasks. In ViTs, the input is processed as patch tokens and then self-attention is used to aggregate spatial information globally (Dosovitskiy et al., 2020). Touvron et al. (2020) explore how to train ViTs efficiently with a distillation strategy. The use of CNNs has a long history for visual tasks, with extensive works conducted on improving the design to aggregate the features from local convolution and enlarge the receptive field.
Different mixing strategies in a feature map: global mixing communicates within all the tokens to gather global spatial information; local mixing mechanism samples neighboring tokens to model local spatial dependency; regional mixing interacts tokens within regions of different scale that is proportional to the relative distance with regards to the query token. Corresponding visualization in view of attention mechanism: the global mixing captures dependency among all tokens, weighted by projection layer; the sparse mixing models local dependency with nearby tokens; our multi-scale regional mixing makes use of fine-grained level information for nearby tokens and coarse-level information for distant tokens.

(LeCun et al., 1998, Krizhevsky et al. 2012, Simonyan & Zisserman 2014, Szegedy et al. 2015, He et al. 2016b). Recent works are proposed to marry the advantages of both global attention in ViTs and local attention in CNNs. PVT (Wang et al., 2021a) exploits a pyramid structure for gathering spatial information on dense prediction tasks such as object detection. TNT (Han et al., 2021) takes small Transformer blocks to capture local information. Swin Transformer (Liu et al., 2021b) proposes shifted window attention in order to aggregate spatial information from local regions. Focal-Transformer (Yang et al., 2021) extends the use of local shifted windows to different scales to efficiently capture both short- and long-range visual dependencies. Incorporating recent findings in Transformers, ConvNeXT (Liu et al., 2022) enlarges the receptive fields with larger kernels to capture global dependencies. Related to these recent progress, our work aims to improve MLP-based architectures to efficiently capture both short-range and long-range visual dependencies.

3 Method

Conventional MLPs are built upon a stacked architecture of multiple token-mixing blocks, where each token-mixing block consists of two sub-blocks, i.e., a spatial-mixing module and a channel-mixing MLP to aggregate spatial and channel information, respectively. Given an input feature with height $H$, width $W$, and channel $C$, expressed as $X \in \mathbb{R}^{H \times W \times C}$, the token-mixing block is formulated as:

$$
Z = f_{Spatial-Mixing}(h_{Spatial}(X)) + X,
$$

$$
O = f_{Channel-Mixing}(h_{Channel}(Z)) + Z,
$$

(1)

where $Z$ and $O$ denote the intermediate feature and output feature of the block, respectively, and $h$ denotes a normalization technique, such as batch normalization or layer normalization (Ioffe & Szegedy, 2015, Ba et al., 2016). The channel-mixing function $f_{Channel-Mixing}$ is usually parameterized with two MLPs, where the hidden dimension of the intermediate output is four times wider than the input dimension. Keeping this setting the same as previous ViTs and MLPs, we focus on investigating the spatial-mixing function $f_{Spatial-Mixing}$ in what follows.
The regional token-mixing can be achieved with a composition of mixing and shifting, where they become dependent compared to conventional methods. Let’s first define three terms to describe the proposed mixing-shifting clearly:

3.1 Multi-scale regional token-mixing

We first provide an illustration of the global and local token-mixing methods, as well as the proposed mixing that interacts tokens within regions on different scales. As shown in Fig. 1, given the query token patch (marked in cobalt blue), global mixing mixes all the tokens in the same channel together to get the output token (marked in cyan); local mixing first samples the tokens in nearby locations from all channels, then mixes them as the output. Correspondingly, in the right panel, the global mixing interacts with all locations and pays attention to all the other tokens, while the local mixing interacts with neighboring tokens of the query and pays attention to the nearby locations. Although global mixing gives interactions with all locations, it is more expensive in computation compared with local mixing, and none of the mixing schemes have the capability to give prioritization to the query. The receptive field of local mixing is also limited as the query only interacts with its neighbors. Here we consider a regional mixing with different region sizes, i.e., 1x1 mixing, 3x3 mixing, 5x5 mixing, 7x7 mixing, and channel MLPs.

Mathematically, with \( x_c \in \mathbb{R}^{H \times W} \) be the c-th channel in X, the global mixing can be formulated as the function \( f_{\text{global}} : \mathbb{R}^{H \times W} \to \mathbb{R}^{H \times W} \) such that \( o_c = f_{\text{global}}(x_c) \), where \( f_{\text{global}} \) is also parameterized with an MLP along the flattened \( H \times W \) dimension (Tolstikhin et al., 2021). In this way, token \( x_{ij,c} \) gathers spatial information from tokens \( \{x_{ij'}(c'), i' \neq i, j' \neq j\} \) located elsewhere. Supposing \( N_{ij} = \mathbb{R}^{H \times W \times C} \subseteq \mathbb{R}^{H \times W \times C} \) denotes the feature map neighboring location of center coordinate \( (i, j) \), local mixing involves a spatial-wise sampling function \( g_{\text{sampling}} \) to get \( N_{ij} \). Then \( f_{\text{local}}(\cdot; i, j) : N_{ij}(\cdot) \to N_{ij}(\cdot) \) mixes the sampled token subset \( \{x_{ij'}(c'), i' \neq i, j' \neq j\} \) such that \( o_{ij,j} = f_{\text{local}}(\{x_{ij'}(c') \in N_{ij}; i', j\}, i, j) \), where \( f_{\text{local}} \) is usually a spatial arrangement operation like shifting or concatenation followed by a channel-wise projection (Yu et al., 2021; Lian et al., 2021).

The proposed regional mixing combines the previous mixing strategies. We regard the sampled tokens \( \{x_{ij'}(c') \in N_{ij}; i', j\} \) as the center tokens of regions with different sizes and deploy a mixing function in each region as \( f_{\text{region}}^r \), where \( f_{\text{region}}^r : \mathbb{R}^{H \times W} \to \mathbb{R}^{H \times W} \), to let the center token represent information in that region, with \( r \) denoting the size of the region. Below we describe this technique in detail.

3.2 Regional token-mixing via mixing and shifting

The regional token-mixing can be achieved with a composition of mixing and shifting, where they become dependent compared to conventional methods. Let’s first define three terms to describe the proposed mixing-shifting clearly:
1) **Shifting size:** We denote $S$ as the shifting size of the feature map. We equally split the input feature along the channel into $S$ groups as $X = x_{C1} \cup \ldots \cup x_{CS}$ and $\forall n \neq m, x_{Cn} \cap x_{Cm} = \emptyset$. We assume the tokens in the first group $x_{C1}$ as queries and shift all the other groups.

2) **Relative distance:** We denote $d_n$ as the relative distance between the query group and each shifted groups $X_{Cn}$. We shift each feature group to reach a relative distance $d_n$ with regards to the query group.

3) **Mixing region size:** We denote $r_n$ as the mixing region size in $X_{Cn}$, where a larger $r_n$ indicates a coarser granularity. Each group will take care of an $r_n \times r_n$ grid region.

Each time, like with local-mixing, we first target a center token $x_{i+d_n,j}$ or $x_{i,j+d_n}$ in each feature group $X_{Cn}$ and mix the tokens in an $r_n \times r_n$ grid region around the center token. Then, we shift the channel groups horizontally or vertically to both align the center tokens and get the features before channel-wise mixing:

$$
\begin{align*}
    y_{i+d_n,j,C_n} &= f_{region}(x_{i+d_n-i+r_n,j-r_n,j+r_n}) \\
    o_{i,j} &= f_{local}(\{y_{i+d_n,j,C_n}\}_{n=1:S}),
\end{align*}
$$

where $f_{region}$ is instantiated with a depth-wise convolution with kernel size $r_n \times r_n$ and $f_{local}$ is a shifting operation.

Fig. 2 shows the architecture of a mix-shifting block and an illustrative example of the proposed mix-shifting. In this example, we set $S = 5, d_n = n - 1$, and $r_n = 2d_n - 1$. In this horizontal mix-shifting, the feature map is divided into five groups, with group C2-C4 gradually increasing both the region size and the relative distance between the center token and the query (cobalt blue token in C1). After the global mixing in each region, each group is shifted back according to the relative distance and all center tokens are aligned for the channel mixing.

### 3.3 Complexity analysis

In this subsection, we compare the computational complexity of typical ways to interact within tokens spatially, including the multi-head self-attention (MSA) in ViTs (Dosovitskiy et al., 2020), window multi-head self-attention (W-MSA) in Swin Transformer (Liu et al., 2021), focal multi-head self-attention (F-MSA) in Focal-Attention Transformer (Yang et al., 2020), global-mixing in MLP-Mixer (Tolstikhin et al., 2021), local-mixing in AS-MLP (Lian et al., 2021), and regional-mixing in our MS-MLP. We assume the channel-MLPs are the same, and that the shifting size and mixing region size in MS-MLP are the same as the focal level and focal region level in F-MSA. Denoting the input dimension as $H \times W \times C$ and the window size of W-MSA and F-MSA as $M$, the complexities of the above methods are shown as follows:

| Method | MSA | W-MSA | F-MSA |
|--------|-----|-------|-------|
| Complexity | $O((2HW)^2C)$ | $O(2M^2HWC)$ | $O((S + \sum_{n=1}^{S} (r_n)^2)MHWC)$ |

| Method | GM | AS | MS |
|--------|----|----|----|
| Complexity | $O((HW)^2C)$ | $O(S)$ | $O(\sum_{n=1}^{S} (r_n)^2)$ |

From Table 1 we can observe that compared with Transformers, MLPs largely reduce the computation complexity in dealing with token dependencies. In the comparison within MLPs, axial-shift and our proposed mix-shifting technique possess much lower complexity than global-mixing in MLP-Mixer. Note that here we make the shifting size $S$ and mixing region size $r_n$ the same as the focal level and focal region size in F-MSA, respectively, for better comparison, meaning each channel group has a different $r_n$. In practice, $r_n$ is not necessarily dependent on $S$, i.e., we can also set a focal level that is smaller than $S$ and the complexity is still $O(\sum_{n=1}^{S} (r_n)^2)$. If we set the focal level to 1 and fix $r_n = 1$, this special case of MS-MLP will reduce to an AS-MLP (Lian et al., 2021).

### 3.4 Model architecture overview

In this part we present an overview of the MS-MLP architecture. Following convention, we consider MS-MLP with Tiny, Small, and Base, corresponding to three different network
Table 2: MS-MLP model architectures with different configurations. Following the convention, we introduce three different configurations—Tiny, Small, and Base—for different model capacities.

| Input resolution | Layer Name | MS-MLP-Tiny | MS-MLP-Small | MS-MLP-Base |
|------------------|------------|-------------|--------------|-------------|
| stage 1 | Patch Embedding | $p_1 = 4; c_1 = 96$ | $p_1 = 4; c_1 = 96$ | $p_1 = 4; c_1 = 128$ |
| stage 2 | MS-block | $S = 5$ | $S = 5$ | $S = 5$ |
| stage 3 | Patch Embedding | $p_2 = 2; c_2 = 192$ | $p_2 = 2; c_2 = 192$ | $p_2 = 2; c_2 = 256$ |
| stage 4 | MS-block | $S = 5$ | $S = 5$ | $S = 5$ |

configurations with different model capacities. Here we follow previous works to adopt a pyramid-like architecture [Wang et al., 2021a; Wu et al., 2021a; Liu et al., 2021b; Yang et al., 2021] [Guo et al., 2021] for our MS-MLP. Our model takes 224 × 224 pixel images as inputs and first splits the input image into patches (tokens) by a patch embedding. Then the token features go through a four-stage architecture. As the features go deeper to another stage, the number of tokens is reduced by a patch-embedding layer with ratio $p_i$ and output channels are simultaneously increased by this ratio. The spatial reduction ratio $p_i$ for these four stages is set as [4, 2, 2, 2]. An overview of three configurations is shown in Table 2. We keep $S = 5$ for all MS-blocks in the architecture for simplicity in presentation, though we believe there should exist a better configuration and we leave it to future exploration. Since the feature map resolution becomes smaller and smaller, we gradually decrease the fine-grained level region mixing. For example, at stage 4 we keep only the channel group with a 7 × 7 region mixing, since in the last stage the patch resolution is sufficiently small. We find the architecture in Table 2 performs the best; we also explored a simpler configuration in our ablations, where all MS-blocks keep the same configuration ($d_n = n − 1$ and $r_n = 2d_n − 1$) and the performance differed very slightly. Moreover, to match the number of parameters and floating-point operations per second (FLOPs) of most existing models, we increase the number of MS-blocks in each stage, but keep the ratio of 1:1:3:1.

3.5 Improving Transformers in low-level stages

How to combine the effectiveness of MLPs in computation with the flexibility of self-attention in Transformers is an interesting topic in computer vision research. In low-level stages, the model needs to process high-resolution inputs. Compared to W-MSA and local-mixing MLPs, MS-MLP has a much larger receptive field coverage; compared to MSA and global-mixing, MS-MLP covers just as many regions, but is more efficient with high-resolution inputs according to our analysis in Section 3.3. We empirically find MS-MLP can be combined with Transformers to boost performance, either by replacing the first-stage architecture or by being added as an additional stage to deal with finer-grained input (e.g., input with patch size 2). In our experiments, we show corresponding improvements over both the Swin Transformer [Liu et al., 2021b] and Focal-Attention Transformer [Yang et al., 2021].

4 Experiments

In this section, we investigate the effectiveness of the MS-MLP architectures using experiments on multiple vision tasks. We first use image classification on ImageNet-1K [Deng et al., 2009] to compare MS-MLP with previous state-of-the-art MLPs. Next, we show the performance of combining MS-MLP with the Swin Transformer [Liu et al., 2021b] and with the Focal-Attention Transformer [Yang et al., 2021], with a comparison to all SoTA methods on this task. Furthermore, we compare MS-MLP with existing alternatives using object detection and semantic segmentation on COCO-2017 [Lin et al., 2014]. Finally, we present ablation
Table 3: Comparison of the proposed MS-MLP architecture with existing vision MLP models on ImageNet. All models are trained and evaluated on $224 \times 224$ resolution, grouped according to the model size. Baseline results are quoted from the original papers.

| Model                  | Mixing  | Params | FLOPs     | Throughput (image / s) | Top-1 acc. (%) |
|------------------------|---------|--------|-----------|------------------------|----------------|
| gMLP-Ti (Liu et al., 2021a) | global  | 6M     | 1.4G      | -                      | 72.3           |
| ResMLP-ST (Touvron et al., 2021) | global  | 15M    | 3.0G      | 1415.1                 | 76.6           |
| CycleMLP-B1 (Chen et al., 2021b) | local   | 15M    | 2.1G      | 1038.4                 | 78.9           |
| Wave-MLP-T (Tang et al., 2021b) | global  | 17M    | 2.4G      | 1208                   | **80.6**       |
| Hire-MLP-T (Guo et al., 2021) | local   | 18M    | 2.1G      | 1561.7                 | 79.7           |
| gMLP-S (Liu et al., 2021a)   | global  | 20M    | 4.5G      | -                      | 79.6           |
| ViP-Small/7 (Hou et al., 2021) | local   | 25M    | -         | 719.0                  | 81.5           |
| AS-MLP-T (Lian et al., 2021)   | local   | 28M    | 4.4G      | 863.6                  | 81.3           |
| CycleMLP-B2 (Chen et al., 2021b) | local   | 27M    | 3.9G      | 640.6                  | 81.6           |
| Wave-MLP-S (Tang et al., 2021b) | global  | 30M    | 4.5G      | 720                    | **82.6**       |
| Hire-MLP-S (Guo et al., 2021) | local   | 33M    | 4.2G      | 1561.7                 | 82.1           |
| MS-MLP-T (ours)            | regional| 28M    | 4.9G      | 792.0                  | 82.1           |
| Mixer-B/16 (Tolstikhin et al., 2021) | global  | 59M    | 12.7G     | -                      | 76.4           |
| S²-MLP-deep (Ya et al., 2021) | local   | 51M    | 10.5G     | -                      | 80.7           |
| ViP-Medium/7 (Hou et al., 2021) | local   | 55M    | -         | 418.0                  | 82.7           |
| CycleMLP-B4 (Chen et al., 2021b) | local   | 52M    | 10.1G     | 320.8                  | 83.0           |
| AS-MLP-S (Lian et al., 2021)   | local   | 50M    | 8.5G      | 478.4                  | 83.1           |
| Wave-MLP-M (Tang et al., 2021b) | global  | 44M    | 7.9G      | 413                    | **83.4**       |
| Hire-MLP-B (Guo et al., 2021) | local   | 58M    | 8.1G      | 440.6                  | 83.2           |
| MS-MLP-S (ours)            | regional| 50M    | 9.0G      | 483.8                  | **83.4**       |
| ResMLP-B24 (Touvron et al., 2021) | global  | 116M   | 23.0G     | 231.3                  | 81.0           |
| S²-MLP-wide (Ya et al., 2021) | local   | 71M    | 14.0G     | -                      | 80.0           |
| CycleMLP-B5 (Chen et al., 2021b) | local   | 76M    | 12.3G     | 246.9                  | 83.2           |
| gMLP-B (Liu et al., 2021a)   | global  | 73M    | 15.8G     | -                      | 81.6           |
| ViP-Large/7 (Hou et al., 2021) | local   | 88M    | -         | 298.0                  | 83.2           |
| AS-MLP-B (Lian et al., 2021)   | local   | 88M    | 15.2G     | 312.4                  | 83.3           |
| Wave-MLP-L (Tang et al., 2021b) | global  | 63M    | 10.2G     | 341                    | 83.6           |
| Hire-MLP-L (Guo et al., 2021) | local   | 96M    | 13.4G     | 290.1                  | **83.8**       |
| MS-MLP-B (ours)            | regional| 88M    | 16.1G     | 366.5                  | **83.8**       |

4.1 Image classification on ImageNet-1K

On ImageNet-1K (Deng et al., 2009), for a fair comparison, we follow the commonly used training recipes in Dosovitskiy et al. (2020) and Wang et al. (2021a). All models are trained for 300 epochs with a batch size of 1,024. The initial learning rate is set to $10^{-3}$ with 20 epochs of linear warm-up starting from $10^{-5}$. For optimization, we use AdamW (Loshchilov & Hutter, 2017) as the optimizer with a cosine learning rate scheduler. The weight decay is set to 0.05 and the maximal gradient norm is clipped to 5.0. We use the same set of data augmentation and regularization strategies as in Touvron et al. (2020), including Rand-Augment (Cubuk et al., 2020), MixUp (Zhang et al., 2017), CutMix (Yun et al., 2019), Label Smoothing (Szegedy et al., 2016), Random Erasing (Zhong et al., 2020), and DropPath (Huang et al., 2016). The stochastic depth drop rates are set to 0.2, 0.3, and 0.5 for our Tiny, Small, and Base models, respectively. During training, we crop images randomly to $224 \times 224$, while a center crop is used during evaluation on the validation set. All models are trained on a node with eight NVIDIA Tesla V100 GPUs, based on which we report the experimental results with top-1 accuracy, number of parameters, FLOPs, and throughput.

Main results comparing with MLPs: We compare the proposed MS-MLP with previous MLP-based models on ImageNet, as shown in Table 3. MS-MLP with region mixing consistently achieves competitive results with better computation efficiency. For example, compared with AS-MLP (Lian et al., 2021) and CycleMLP (Chen et al., 2021b), MS-MLP can perform significantly better with comparable parameter scales, FLOPs, and throughput. When compared with recently proposed Wave-MLP (Tang et al., 2021b) and Hire-MLP (Guo et al., 2021), MS-MLP obtains a better throughput and similar classification accuracy. In particular, scale up to Base configuration, MS-MLP achieves the best results (83.8%) with a
Table 4: Comparison of MS-MLP architecture with representative SoTA models on ImageNet-1K with a resolution of 224 × 224.

| Model                   | Family | Params. | FLOPs   | Throughput (images / s) | Top-1 acc. (%) |
|-------------------------|--------|---------|---------|-------------------------|----------------|
| ResNet18                | CNN    | 12M     | 1.8G    | -                       | 69.8           |
| ResNet50                | CNN    | 26M     | 4.1G    | -                       | 78.5           |
| ResNet101               | CNN    | 45M     | 7.9G    | -                       | 79.8           |
| ConvNeXt-T (Liu et al., 2022) | CNN | 29M  | 4.5G  | 775                     | 82.1           |
| ConvNeXt-S (Liu et al., 2022) | CNN | 50M  | 8.7G  | 447                     | 83.1           |
| ConvNeXt-B (Liu et al., 2022) | CNN | 89M  | 15.4G | 292                     | 83.8           |
| Swin-T (Liu et al., 2021b) | Trans | 29M  | 4.5G  | 755                     | 81.3           |
| Swin-S (Liu et al., 2021b) | Trans | 50M  | 8.7G  | 437                     | 83.0           |
| Swin-B (Liu et al., 2021b) | Trans | 88M  | 15.4G | 278                     | 83.3           |
| Focal-Attention-T (Yang et al., 2021) | Trans | 29M | 4.9G | 319                     | 82.2           |
| Focal-Attention-S (Yang et al., 2021) | Trans | 52M | 9.4G | 192                     | 83.5           |
| Focal-Attention-B (Yang et al., 2021) | Trans | 90M | 16.4G | 138                     | 83.8           |
| MS-MLP-T (ours)         | MLP    | 29M     | 4.5G    | 779                     | 81.9           |
| MS-MLP-S (ours)         | MLP    | 50M     | 8.7G    | 464                     | 83.5           |
| MS-MLP-B (ours)         | MLP    | 88M     | 15.4G   | 279                     | 83.8           |

Comparing with SoTAs: Besides MLPs, we compare MS-MLP with representative CNN-based and Transformer-based SoTA models. The input image resolution is set as 224 × 224. As in Table 4, compared with SoTAs, MS-MLP achieves competitive performance with better efficiency. For example, MS-MLP-B achieves 83.8% top-1 accuracy, which is superior to Swin-B with 83.3% accuracy. The computational efficiency of MS-MLP is significantly better than Transformers, and slightly surpasses the CNN architectures like ConvNeXt (Liu et al., 2022).

Table 5: Comparison of Swin and Focal-Attention transformer w/o MS-MLP on ImageNet-1K.

| Model                   | Family | Params. | FLOPs   | Throughput (images / s) | Top-1 acc. (%) |
|-------------------------|--------|---------|---------|-------------------------|----------------|
| Swin-T (Liu et al., 2021b) | Trans | 29M  | 4.5G  | 755                     | 81.3           |
| Swin-S (Liu et al., 2021b) | Trans | 50M  | 8.7G  | 437                     | 83.0           |
| Swin-B (Liu et al., 2021b) | Trans | 88M  | 15.4G | 278                     | 83.3           |
| MS-MLP + Swin-T (ours)  | MLP + T | 29M | 4.5G | 779                     | 81.9           |
| MS-MLP + Swin-S (ours)  | MLP + T | 50M | 8.7G | 464                     | 83.5           |
| MS-MLP + Swin-B (ours)  | MLP + T | 88M | 15.4G | 279                     | 83.8           |
| Focal-Attention-T (Yang et al., 2021) | Trans | 29M | 4.9G | 319                     | 82.2           |
| Focal-Attention-S (Yang et al., 2021) | Trans | 52M | 9.4G | 192                     | 83.5           |
| Focal-Attention-B (Yang et al., 2021) | Trans | 90M | 16.4G | 138                     | 83.8           |
| MS-MLP + Focal-Attention-T (ours) | MLP + T | 29M | 5.6G | 451                     | 82.8           |
| MS-MLP + Focal-Attention-S (ours) | MLP + T | 52M | 10.1G | 297                     | 83.9           |
| MS-MLP + Focal-Attention-B (ours) | MLP + T | 90M | 17.6G | 207                     | 84.0           |

Results with Transformers: To effectively combine the strengths of both MS-MLP and Transformers, we let MS-MLP and Transformers represent low-level and high-level stages, respectively. We found this design can largely boost model efficiency. In the experiments, we replace the first stage of the Swin Transformer (Liu et al., 2021b) and the Focal-Attention Transformer (Yang et al., 2021) with MS-blocks. Moreover, we add a stage zero that consists of two MS-blocks with $p_0 = 2$, $c_0 = c_1/2$ ahead of stage one. This novel configuration produces a modified model having similar parameter sizes, FLOPs, and throughputs as the original models, but a consistently better performance in terms of accuracy.

We compare the proposed MS-MLP+Transformer architecture with the original architectures on ImageNet-1K and summarize the results in Table 5. Compared with the Swin Transformer and Focal-Attention Transformer, the MS-MLP+Transformer architectures achieve both a higher accuracy and a higher throughput with a similar number of parameters and FLOPs. For example, with 88M parameters and 15.4G FLOPs, MS-MLP+Swin-B throughput (366.5 images/sec) surpassing all the other models with a comparable number of parameters.
achieves an 83.8% top-1 accuracy, surpassing Swin-B with 83.3% accuracy. With very similar 90M parameters and slightly higher FLOPs, MS-MLP+Focal-Attention improves both the top-1 classification accuracy and the throughputs, e.g., the latest Baseline-2. The superiority of MS-MLP+Transformer clearly implies that the MS-MLP architecture has a better efficiency in the token aggregation process. This positive effect becomes more pronounced with larger token sizes, since the proposed mixing and shifting operations can exploit both global and local dependencies adequately.

4.2 Object detection and instance segmentation

**Results on COCO-2017**: We first conduct the object detection and instance segmentation experiments on COCO-2017 (Lin et al., 2014). Following previous works (Wang et al., 2021a; Liu et al., 2021), we use the pretrained models as backbones and plug into RetinaNet (Lin et al., 2017), Mask R-CNN (He et al., 2017), and Cascade Mask R-CNN (Chai & Vasconcelos, 2018) in mmdetection (Chen et al., 2019). We adopt the single-scale and multi-scale training for the “1x” and “3x” schedules, respectively.

The results of object detection and instance segmentation with different frameworks and training schedules are reported in Table 6 and Table 11 (Appendix), respectively. As shown in Table 6, using MS-MLP as the backbone, RetinaNet and Mask R-CNN surpass most of the MLP-based baselines. For example, compared to recent MLPs, MS-MLP outperforms Hire-MLP-L and WaveMLP-B by 0.6% and 1.5%, respectively, on RetinaNet. In downstream tasks like object detection and segmentation, Hire-MLP-L and Wave-MLP-B usually require high-resolution input and both short- and long-range token interactions. Our regional mixing shows the effectiveness from this perspective, compared to the global-only or local-only token interactions.

**Results on ADE20K**: Besides the detection and instance segmentation tasks, we further evaluate our model on semantic segmentation, where we use UperNet (Xiao et al., 2018) with our pretrained models as the backbone. For all models, we use a standard recipe by

Table 6: Results of detection and instance segmentation on COCO val2017. We compare MS-MLP with other backbones based on RetinaNet and Mask R-CNN frameworks. All models are trained on the “1x” schedule.

| Backbone                  | Param / FLOPs          | RetinaNet 1x | Mask R-CNN 1x |
|---------------------------|------------------------|--------------|--------------|
|                           | AP         | AP$_{50}$ | AP$_{75}$ | AP$_{m}$    | AP$_{50}$ | AP$_{75}$ | AP$_{m}$ |
| CycleMLP-B2 (Chen et al., 2021) | 36.5M / 215G | 40.9 | 24.1 | 47.4 | 53.4 | 46.5M / 226G | 41.7 | 36.3 | 45.8 | 38.2 | 60.4 | 41.0 |
| Wave-MLP-S (Yang et al., 2020) | 37.1M / 211G | 43.4 | 26.6 | 47.1 | 57.1 | 47.0M / 225G | 42.0 | 35.7 | 48.0 | 38.0 | 63.1 | 42.9 |
| Hire-MLP-S (Guo et al., 2021)  | 44.5M / 227G | 51.7 | 33.3 | 54.4 | 60.4 | 52.7M / 228G | 43.2 | 40.0 | 56.0 | 39.3 | 62.0 | 42.1 |
| MS-MLP-T (ours)            | 49.6M / 240G | 52.7 | 26.0 | 47.3 | 59.7 | 49.8M / 229G | 44.4 | 47.5 | 52.8 | 40.4 | 61.3 | 44.2 |
| CycleMLP-S (Chen et al., 2021) | 48.0M / 210G | 47.2 | 25.2 | 45.3 | 58.2 | 48.0M / 209G | 43.4 | 40.0 | 47.4 | 39.5 | 62.0 | 42.4 |
| CycleMLP-B3 (Chen et al., 2021) | 41.5M / 266G | 43.2 | 26.6 | 46.5 | 57.4 | 44.1 | 41.0 | 46.1 | 39.2 | 62.7 | 43.5 |
| Wave-MLP-M (Yang et al., 2020) | 49.4M / 214G | 44.8 | 28.0 | 48.2 | 59.4 | 50.9M / 231G | 53.0 | 47.3 | 49.0 | 41.0 | 61.4 | 44.1 |
| Hire-MLP-B (Guo et al., 2021)  | 60.0M / 236G | 52.3 | 28.0 | 48.4 | 58.9 | 77.8M / 304G | 54.5 | 46.9 | 49.3 | 41.0 | 64.0 | 44.2 |
| MS-MLP-S (ours)            | 61.0M / 246G | 51.0 | 28.0 | 48.9 | 60.4 | 70.9M / 375G | 47.1 | 47.1 | 51.0 | 41.9 | 64.1 | 45.1 |
| CycleMLP-S-B (Chen et al., 2021) | 85.9M / 402G | 59.1 | 24.7 | 46.4 | 57.4 | 95.3M / 423G | 47.4 | 59.3 | 51.5 | 41.8 | 69.3 | 44.0 |
| Wave-MLP-B (Yang et al., 2020) | 68.1M / 343G | 57.2 | 33.0 | 45.1 | 59.9 | 75.1M / 375G | 54.7 | 47.0 | 49.2 | 48.4 | 64.0 | 48.4 |
| Hire-MLP-L (Guo et al., 2021)  | 105.8M / 448G | 54.9 | 28.9 | 48.9 | 57.5 | 115.2M / 443G | 65.9 | 57.0 | 50.4 | 43.7 | 64.7 | 45.3 |
| MS-MLP-L (ours)            | 97.5M / 544G | 57.7 | 27.6 | 49.0 | 59.8 | 107.0M / 557G | 46.4 | 47.2 | 50.7 | 42.4 | 63.6 | 46.4 |

Table 7: Results of semantic segmentation on the ADE20K validation set. FLOPs are calculated with an input size of 2048×512.

| Backbone                  | Param | FLOPs | SS mIoU | MS mIoU |
|---------------------------|-------|-------|---------|---------|
| Swin-T (Liu et al., 2021) | 60M   | 945G  | 44.5    | 46.1    |
| Focal-T (Yang et al., 2022) | 62M   | 980G  | 45.8    | 47.0    |
| AS-MLP-L (Comae et al., 2021) | 60M   | 937G  | 44.5    |         |
| Hire-MLP-S (Guo et al., 2021) | 63M   | 930G  | 46.1    | 47.1    |
| MS-MLP-T (ours)           | 60M   | 939G  | 46.0    | 46.8    |
| ResNet-101 (He et al., 2016) | 86M   | 1029G | 43.8    | 44.9    |
| Swin-S (Liu et al., 2021) | 81M   | 1036G | 47.6    | 49.5    |
| Focal-S (Yang et al., 2021) | 85M   | 1130G | 48.6    | 50.0    |
| AS-MLP-S (Lan et al., 2021) | 81M   | 1024G | 49.2    |         |
| Hire-MLP-B (Chai & Vasconcelos, 2018) | 86M | 1011G | 48.3    | 49.6    |
| MS-MLP-S (ours)           | 82M   | 1028G | 48.7    | 49.6    |
| Swin-B (Liu et al., 2021) | 121M  | 1188G | 48.1    | 49.7    |
| Focal-B (Yang et al., 2021) | 126M  | 1345G | 49.0    | 50.5    |
| AS-MLP-B (Lan et al., 2021) | 121M  | 1166G | 49.5    |         |
| Hire-MLP-L (Chai & Vasconcelos, 2018) | 127M | 1125G | 48.8    | 49.9    |
| MS-MLP-B (ours)           | 122M  | 1172G | 49.1    | 49.9    |
Table 8: Analogous comparison to Table 6 between using MS-MLP plugged-in Transformer architecture and their original architectures.

| Backbone | RetinaNet 1x | Mask R-CNN 1x |
|----------|--------------|---------------|
|          | Param / FLOPs | AP  | AP 50 | AP 75 | AP 90 | AP 50 | AP 75 | AP 90 | AP 50 | AP 75 | AP 90 |
| Swin-T [Liu et al., 2021] | 58.8M / 336G | 41.5 | 35.1 | 30.1 | 25.5 | 47.8M / 269G | 64.2 | 60.6 | 57.2 | 53.1 | 61.6 | 58.1 |
| Swin-T [Liu et al., 2021] | 62.0M / 354G | 44.8 | 39.4 | 34.4 | 30.0 | 44.8M / 299G | 66.6 | 62.0 | 58.9 | 54.9 | 64.6 | 61.5 |
| Swin-S [Liu et al., 2021] | 99.9M / 544G | 45.2 | 39.5 | 34.5 | 30.0 | 99.9M / 539G | 69.6 | 65.0 | 61.8 | 57.3 | 69.3 | 65.6 |
| Swin-S [Liu et al., 2021] | 100.8M / 554G | 45.2 | 39.5 | 34.5 | 30.0 | 100.8M / 549G | 72.7 | 68.0 | 62.3 | 58.8 | 70.3 | 66.4 |

Table 9: Configurations of different $r_n$ and $d_n$ of MS-MLP.

| Configs | Local | Global | Isolated Regional | Regional |
|---------|-------|--------|-------------------|----------|
| $r_{1,8}$ | $[1, 1, 1, 1]$ | $[1, 1, 1, 1]$ | $[1, 1, 3, 5]$ | $[1, 1, 3, 5]$ |
| $d_{1,8}$ | $[0, 1, 2, 3, 4]$ | $[0, 1, 2, 3, 4]$ | $[0, 2, 5, 10, 17]$ | $[0, 1, 2, 3, 4]$ |

Table 10: Comparison of different patch size on ImageNet-1K.

| Method     | Patch size | Accuracy |
|------------|------------|----------|
| Swin-T     | 2          | 81.4%    |
|            | 4          | 81.3%    |
| MS-MLP+Swin-T | 2          | 81.9%    |
|            | 4          | 81.6%    |

setting the input size as 512 × 512 and train the model for 160k iterations with a batch size of 16. The results are shown in Table 7. We can observe that MS-MLP achieves better single-scale mIoUs than the baselines and has competitive multi-scale mIoUs across different model capacities.

Results with Transformers: Similar to the classification tasks, we validate the effectiveness of combining MS-MLP with the Swin and Focal-Attention Transformers on COCO-2017 object detection and instance segmentation using their original settings. Table 8 shows an analogous comparison to Table 6 for this task. The MS-MLP+Transformer backbone improves their original Transformer backbones by 0.5-0.7% on both RetinaNet and Mask-RCNN.

4.3 Ablation studies

We conduct ablation studies using MS-MLP-Tiny by varying the region mixing size $r_n$ and relative distance $d_n$ to validate the effectiveness of regional mixing. We propose four different configurations as shown in Table 9: 1) all regional mixing sizes are restricted to 1 to achieve local mixing. This keeps only the shifting module and is close to AS-MLP [Lian et al., 2021]. 2) All region sizes are set to 7 to cover as many tokens as possible. This setting aims to approximate the global mixing and is also related to W-MSA in Swin [Liu et al., 2021b]. 3) We set the region to a different granularity but enlarge the shifting step size to let each region be isolated from each other. 4) The proposed regional mixing.

We show the classification results with inputs that have a patch size of 2 or 4 in Fig. 3. As we can see, only using local or global mixing has a lower performance than regional mixing. Especially, for global mixing without the self-attention mechanism, token-mixing becomes less flexible to capture important information. We observe the performance is even lower when the patch size is 2. For the isolated setting, without interactions within regions, information from different regions is hard to collect. This isolated mixing is even less effective than using local information. When the patch size is 2, the number of input tokens becomes larger. We can see local and regional mixings both leverage finer-grained information improving classification accuracy, with significant improvements in regional mixing. This continues to validate the effectiveness of the regional mixing.

When combining MS-MLP with Transformers, we inject MS-MLP in both stages 0 and 1 of the Transformer to match the model parameters and throughputs. We study whether the Transformer itself can benefit from smaller input patches. We show a comparison between Swin-T and MS-MLP+Swin-T in Table 10 where we can see smaller patch inputs only improve Swin-T by 0.1%. However, the improvements from MS-MLP are more significant for both patch size 2 (81.4% vs. 81.9%) and 4 (81.3% vs. 81.6%).
5 Conclusion

In this paper, we present a regional mixing method via mixing and shifting operations to enable an efficient modeling of local-global dependency in MLPs. MS-MLP performs the token mixing at both fine-grain and coarse-grain levels, effectively handling both local and global dependencies with low computational cost. Extensive experiments show the effectiveness of MS-MLP over SoTA MLPs and other representative SoTA methods on both image classification and object detection and segmentation.

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A Experiment settings

A.1 Image classification on ImageNet-1K

Following the settings of the Swin transformer (Liu et al., 2021b), image classification is performed by applying an adaptive global average pooling layer on the output feature map of the last stage followed by a linear classifier. In evaluation, the top-1 accuracy using a single crop is reported.

The training settings mostly follow the Swin transformer (Liu et al., 2021b) and AS-MLP (Lian et al., 2021). For all model variants, we adopt a default input image resolution of $224 \times 224$. When training from scratch with an input of size $224 \times 224$, we employ an AdamW (Loshchilov & Hutter, 2017) optimizer for 300 epochs using a cosine decay learning rate scheduler with 20 epochs of linear warm-up. Keeping a batch size of 1,024, an initial learning rate of 0.001, a weight decay of 0.05, and a gradient clipping with a max norm of 1 are used. We include most of the augmentation and regularization strategies of (Touvron et al., 2020) in training, including Rand-Augment (Cubuk et al., 2020), MixUp (Zhang et al., 2017), CutMix (Yun et al., 2019), Label Smoothing (Szegedy et al., 2016), Random Erasing (Zhong et al., 2020), and DropPath (Huang et al., 2016). Different from the Swin and Focal-Attention Transformer, we empirically find the Exponential Moving Average (EMA) (Polyak & Juditsky, 1992) can enhance performance, but for a fair comparison we did not report the EMA results in the paper. An increasing degree of stochastic depth augmentation is employed for larger models, i.e., 0.2, 0.3, 0.5 for MLP-T, MLP-S, and MLP-B, respectively.

A.2 Downstream tasks: Object detection on COCO and semantic segmentation on ADE20K

On COCO-2017 tasks, we consider four typical object detection frameworks: RetinaNet (Lin et al., 2017), Mask R-CNN (He et al., 2017), and Cascade Mask R-CNN (Cai & Vasconcelos, 2018) in mmdetection (Chen et al., 2019). We utilize the single-scale training and multi-scale training for the “1x” and “3x” (resizing the input such that the shorter side is between 480 and 800 while the longer side is at most 1,333) schedules, respectively. For these frameworks, we utilize the same settings where we adopt the AdamW optimizer (Loshchilov & Hutter, 2017) (initial learning rate of 0.0001, weight decay of 0.05, and a batch size of 16), and “3x” schedule (36 epochs with the learning rate decayed by 10× at epochs 27 and 33).

On ADE20K (Zhou et al., 2019), which contains 20,210 training images and 2,000 validation images, we conduct semantic segmentation experiments following the settings in (Wang et al., 2021a; Chen et al., 2021b; Liu et al., 2021b). We use UperNet (Xiao et al., 2018) as the segmentation framework and a pretrained MS-MLP as the backbone. For all models, we use a standard recipe by setting the input size to 512 × 512 and train the model for 160k iterations with a batch size 16 in the training. We follow the training settings described in Liu et al. (2021b), where we employ the AdamW optimizer (Loshchilov & Hutter 2017) with an initial learning rate of $6 \times 10^{-5}$, a weight decay of 0.01, a scheduler that uses linear learning rate decay, and a linear warmup of 1,500 iterations. For augmentations, we adopt the default setting in mmsegmentation (Contributors, 2020) of random horizontal flipping, random re-scaling within ratio range $[0.5, 2.0]$, and random photometric distortion. Stochastic depth with ratio of 0.2 is applied for all models.

B Additional Experiment Results.

B.1 Instance segmentation with 3x schedule

For the object detection and instance segmentation tasks on COCO-2017, we also train models with 3x schedule and multi-scale training strategy as described in the main experiments. The results of Mask R-CNN (He et al., 2017) and Cascade Mask R-CNN (Cai & Vasconcelos, 2018) are shown in Table 11. Similar to the results in the “1x” schedule, the proposed MS-MLP achieves a higher performance.
Table 11: Instance segmentation results on COCO val2017. Mask R-CNN and Cascade Mask R-CNN are trained on the “3x” schedule.

| Backbone                  | Mask R-CNN 3x | Cascade Mask R-CNN 3x |
|---------------------------|---------------|-----------------------|
|                           | FLOPs | AP | AP50 | AP75 | AP | AP50 | AP75 | AP | AP50 | AP75 |
| ResNet50 (He et al., 2016b) | 260G  | 41.0 | 61.7 | 44.9 | 37.1 | 58.4 | 40.1 | 50.5 | 61.7 | 43.4 |
| AS-MLP-T (Lian et al., 2021) | 260G  | 46.0 | 67.5 | 50.7 | 41.5 | 64.6 | 44.5 | 50.1 | 68.8 | 43.5 |
| Swin-T (Liu et al., 2021b) | 264G  | 46.0 | 68.2 | 50.2 | 41.6 | 65.1 | 44.8 | 50.5 | 69.3 | 43.7 |
| Hire-MLP-Small (Guo et al., 2021) | 256G  | 46.2 | 68.2 | 50.9 | 42.0 | 65.6 | 45.3 | 50.7 | 69.4 | 44.2 |
| MS-MLP-T (ours)           | 262G  | 46.2 | 67.8 | 50.8 | 41.7 | 65.2 | 45.0 | 50.4 | 69.2 | 43.7 |
| AS-MLP-S (Lian et al., 2021) | 346G  | 47.8 | 68.9 | 52.5 | 42.9 | 64.6 | 44.5 | 51.1 | 69.8 | 55.6 |
| Hire-MLP-S (ours)         | 334G  | 48.1 | 69.6 | 52.7 | 41.1 | 66.8 | 46.7 | 51.7 | 70.2 | 56.1 |
| AS-MLP-S (Lian et al., 2021) | 424G  | 48.6 | 70.8 | 53.4 | 43.7 | 67.7 | 47.2 | 51.9 | 70.8 | 56.6 |
| MS-MLP-S (ours)           | 561G  | 49.0 | 70.0 | 52.6 | 43.7 | 65.4 | 46.7 | 52.6 | 71.4 | 57.2 |
| Swin-B (Liu et al., 2021b) | 496G  | 48.5 | 70.2 | 53.5 | 43.3 | 67.3 | 46.6 | 51.9 | 71.8 | 57.5 |
| MS-MLP-B (ours)           | 424G  | 48.6 | 70.8 | 53.4 | 43.7 | 67.3 | 46.6 | 51.9 | 71.8 | 57.5 |

B.2 Image classification with different architecture

In the main paper we set the MS-MLP in an architecture with four-stages, where the number of blocks keeps a ratio of 1:1:3:1. To match the parameter size and throughputs, these stages contain 3-3-9-3 blocks for MS-MLP-T and 3-3-27-3 for MS-MLP-S and MS-MLP-B. We also match the architecture with Swin (Liu et al., 2021b) and AS-MLP (Lian et al., 2021), using the stage design of 2-2-6-2 for MS-MLP-T and 2-2-18-2 for MS-MLP-S and MS-MLP-B. The results are summarized in Table 12. We can see the results are comparable to the results shown for Swin (Liu et al., 2021b) and AS-MLP (Lian et al., 2021), while the parameter size and FLOPs are fewer.

For the regional mixing, we choose to use depth-wise convolution with different kernel size. We conduct experiments to see the effects of the kernel sizes and convolution type as an additional ablation. In Table 13, we can observe the full convolution has no special effects to the final results, while using full convolution increases the FLOPs and slows down the training. We also observe slightly changing the kernel size does not affect the results. However, the results show that decreasing the region size while the relative distance increases degrades model performance.

Table 12: Image classification results of different architecture MS-MLP.

| Model     | Blocks | #Parameters | FLOPs | Top-1 acc. |
|-----------|--------|-------------|-------|------------|
| MS-MLP-T  | 2-2-6-2 | 24M         | 4.3G  | 81.4%      |
|           | 2-2-6-2 | 24M         | 4.4G  | 81.3%      |
| MS-MLP-S  | 2-2-18-2 | 42M         | 7.8G  | 82.8%      |
|           | 2-2-18-2 | 42M         | 7.8G  | 83.0%      |
| MS-MLP-B  | 2-2-18-2 | 74M         | 13.8G | 83.3%      |
|           | 2-2-18-2 | 74M         | 13.9G | 83.2%      |

Table 13: Image classification results of different MS-block configurations.

| Region size | Conv type | FLOPs | Top-1 acc. |
|-------------|-----------|-------|------------|
| 1-1-3-5-7   | DW        | 4.9G  | 82.1%      |
| 1-1-3-5-7   | Full      | 7.7G  | 82.0%      |
| 1-3-5-7-9   | DW        | 5.6G  | 81.8%      |
| 1-3-5-7-9   | Full      | 9.1G  | 82.0%      |
| 1-7-5-3-1   | DW        | 4.9G  | 81.1%      |
| 1-7-5-3-1   | Full      | 7.7G  | 81.3%      |
| 1-5-3-3-1   | DW        | 4.6G  | 81.2%      |
| 1-5-3-3-1   | Full      | 6.8G  | 81.4%      |

C More discussion and limitations

We demonstrate MS-MLP can perform as well as representative ViTs and CNNs on image classification, object detection, instance, and semantic segmentation tasks. While our goal is to offer a general way to handle global and local visual dependencies, MS-MLP still relies on a careful choice of the region size and the relative shifting distance, and we are not able to explore all possible configurations. As we realize computer vision applications are diverse, the current MS-MLP configuration may be suited for certain tasks, and we may need to explore a more general recipe for other tasks.
Table 14: Full comparison of MS-MLP architecture with SOTA models on ImageNet-1K.

| Model                          | Family | Params. | FLOPs | Throughput (image / s) | Top-1 acc. (%) |
|--------------------------------|--------|---------|-------|-------------------------|----------------|
| ResNet18 [He et al., 2016a]    | CNN    | 12M     | 1.8G  | -                       | 69.8           |
| ResNet50 [He et al., 2016a]    | CNN    | 26M     | 4.1G  | -                       | 78.5           |
| ResNet101 [He et al., 2016a]   | CNN    | 45M     | 7.9G  | -                       | 79.8           |
| RegNetY-4G [Radosavovic et al., 2020] | CNN | 21M     | 4.0G  | 1157                    | 80.0           |
| RegNetY-8G [Radosavovic et al., 2020] | CNN | 39M     | 8.0G  | 592                     | 81.7           |
| RegNetY-16G [Radosavovic et al., 2020] | CNN | 84M     | 16.0G | 335                     | 82.9           |
| ConvNeXt-T [Liu et al., 2022]  | CNN    | 29M     | 4.5G  | 774.7                   | 82.1           |
| ConvNeXt-S [Liu et al., 2022]  | CNN    | 50M     | 8.7G  | 447.1                   | 83.1           |
| ConvNeXt-B [Liu et al., 2022]  | CNN    | 89M     | 15.4G | 292.1                   | 83.8           |
| GFNet-H-S [Rao et al., 2021]   | FFT    | 32M     | 4.5G  | -                       | 81.5           |
| GFNet-H-B [Rao et al., 2021]   | FFT    | 54M     | 8.4G  | -                       | 82.9           |
| DeiT-S [Touvron et al., 2020]  | Trans  | 22M     | 4.6G  | 940                     | 79.8           |
| DeiT-B [Touvron et al., 2020]  | Trans  | 86M     | 17.5G | 292                     | 81.8           |
| PVT-Small [Wang et al., 2021b] | Trans  | 25M     | 3.8G  | 820                     | 79.8           |
| PVT-Medium [Wang et al., 2021b] | Trans | 44M     | 6.7G  | 526                     | 81.2           |
| PVT-Large [Wang et al., 2021b] | Trans  | 61M     | 9.8G  | 367                     | 81.7           |
| T2T-VIT-14 [Yuan et al., 2021] | Trans  | 22M     | 5.2G  | 764                     | 81.5           |
| T2T-VIT-19 [Yuan et al., 2021] | Trans  | 39M     | 8.9G  | 464                     | 81.9           |
| T2T-VIT-24 [Yuan et al., 2021] | Trans  | 64M     | 14.1G | 312                     | 82.3           |
| TNT-S [Han et al., 2021]       | Trans  | 24M     | 5.2G  | 428                     | 81.5           |
| TNT-B [Han et al., 2021]       | Trans  | 66M     | 14.1G | 246                     | 82.9           |
| iRPE-K [Wu et al., 2021]       | Trans  | 87M     | 17.7G | -                       | 82.4           |
| iRPE-QKV [Wu et al., 2021]     | Trans  | 22M     | 4.9G  | -                       | 81.4           |
| GLiT-Small [Chen et al., 2021a] | Trans  | 25M     | 4.4G  | -                       | 80.5           |
| GLiT-Base [Chen et al., 2021a] | Trans  | 96M     | 17.0G | -                       | 82.3           |
| MS-MLP-T (ours)                | MLP    | 28M     | 4.9G  | 792                     | 82.1           |
| MS-MLP-S (ours)                | MLP    | 50M     | 9.0G  | 484                     | 83.4           |
| MS-MLP-B (ours)                | MLP    | 88M     | 16.1G | 366                     | 83.8           |
| Swin-T [Liu et al., 2021b]     | Trans  | 29M     | 4.5G  | 755                     | 81.3           |
| MS-MLP + Swin-T (ours)         | MLP + T| 29M     | 4.5G  | 779                     | 81.9 (+0.6)    |
| Swin-S [Liu et al., 2021b]     | Trans  | 50M     | 8.7G  | 437                     | 83.0           |
| MS-MLP + Swin-S (ours)         | MLP + T| 50M     | 8.7G  | 464                     | 83.5 (+0.5)    |
| Swin-B [Liu et al., 2021b]     | Trans  | 88M     | 15.4G | 278                     | 83.3           |
| MS-MLP + Swin-B (ours)         | MLP + T| 88M     | 15.4G | 279                     | 83.8 (+0.5)    |
| Focal-Attention-T [Yang et al., 2021] | Trans | 29M     | 4.9G  | 319                     | 82.2           |
| MS-MLP + Focal-Attention-T (ours) | MLP + T| 29M     | 5.6G  | 451                     | 82.8 (+0.6)    |
| Focal-Attention-S [Yang et al., 2021] | Trans | 52M     | 9.4G  | 192                     | 83.5           |
| MS-MLP + Focal-Attention-S (ours) | MLP + T| 52M     | 10.1G | 297                     | 83.9 (+0.4)    |
| Focal-Attention-B [Yang et al., 2021] | Trans | 90M     | 16.4G | 138                     | 83.8           |
| MS-MLP + Focal-Attention-B (ours) | MLP + T| 90M     | 17.0G | 207                     | 84.0 (+0.2)    |