Real-time and -space visualization of excitations of the $\nu = 1/3$ fractional quantum Hall edge

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We present scanning optical stroboscopic confocal microscopy and spectroscopy measurements wherein three degrees of freedom, namely energy, real-space, and real-time, are resolvable. The edge-state propagation is detected as a temporal change in the optical response in the downstream edge. We succeeded in visualizing the excited states of the most fundamental fractional quantum Hall (FQH) state and the collective excitations near the edge. The results verify the current understanding of the edge excitation and also point toward further dynamics outside the edge channel.

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When electrons confined to two dimensions (2D) are subjected to a perpendicular magnetic field $B$, and the ratio of their density $n_e$ and the flux quanta density (i.e., $\nu$, the Landau-level filling factor) is an integer or rational fraction, the bulk of the system develops a gap to form integer and fractional quantum Hall (QH) states. Herein, $\nu = \frac{h}{eB} n_e$, where $h$ and $e$ denote the Planck’s constant and elementary charge, respectively. The QH system is the most extensively studied 2D topological material [1–4] wherein the bulk of the system comprises an insulator, and electric conduction is restricted to the edge. Because $B$ breaks the time-reversal symmetry, the one-dimensional (1D) edge current, i.e., edge-state excitations called edge magneto-plasmons (EMPs) [5], propagates unidirectionally. In contrast to the bulk, the system edge contains compressible regions with a gapless excitation. This QH edge state constitutes a 1D system that exhibits uniquely high coherence [6] and hosts a wide variety of physics [7–13], such as the Tomonaga-Luttinger liquid [12–13], anyonic statistics [14–15], and charge-neutral upstream Majorana modes of the edge current [7]. Furthermore, it offers the potential for exotic applications, including topological and flying qubit quantum computation [10–13, 18, 19] and quantum energy teleportation [19–21]. The properties of these edge states are typically examined through electric measurements [6–13, 18, 19, 22], including shot-noise [6–8] and heat-transport measurements [4]. The edge current dynamics have been specifically examined by time-resolved transport measurements [19–21]. In general, measurements that detect electric signals from electrodes attached to a sample are limited in that they only obtain information from a certain fixed region. By contrast, scanning optical microscopy can quantify the properties of the electronic system, such as spin polarization, in the spatial domain [23, 24]. This is because the intensity and photon energy of photoluminescence (PL) emitted from the bound states of two electrons and a hole, known as charged excitons or trions, are highly sensitive to the electronic environment around the trions [22, 25] [see Supplementary Material (SM)].

To explore the edge-state dynamics in real space and time, we performed scanning confocal microscopy and spectroscopy experiments using a stroboscopic technique known as temporal aliasing (Fig. 1). Our scanning confocal microscopy apparatus collects light from illuminated 2D electrons in a 15-nm GaAs/AlGaAs quantum well (QW) (see SM details regarding the sample). A mode-locked Ti:sapphire laser pulse is transmitted through an optical fiber and low-temperature optics, and focused on a selected position of the sample to microscopically excite trions. The resulting microscopic PL spectra are col-
selected through the objective lens and fiber, and then sent to a spectrometer and measured using a charge-coupled device (CCD) detector. The low-temperature optics partially depicted in Fig. 1 comprise mirrors, a polarizing beam splitter, a λ/4 wave plate, and an objective lens. They are located near the sample, and are used to focus the laser and selectively collect the σ−-polarized PL. They are located near the sample, and are used to focus the laser and selectively collect the σ−-polarized PL. The PL collected from the sample is transmitted through the same fiber and introduced to the monochromator and CCD. The focal point of the confocal microscope can be aligned to the sample surface and scanned across the sample in 2D by piezoelectric stages (See SM for details for the scanning optical microscopy).

A laser pulse is synchronized to a voltage pulse applied to the excitation gate deposited on top of the sample [19] (Figs. 1, 4(a), and S1) with a controllable time delay ∆t. This ensures that the measured PL reflects the electronic state at a moment following the voltage pulse. This pulse creates a local charge disturbance that propagates as an EMP wave packet [10–13, 19] along the boundary of the QH system defined by the interface of the QW and the vacuum. For a specific ∆t, the wave packet arrives at the laser focal point in coincidence with the laser pulse illumination. This allows us to capture the PL spectra reflecting the electronic state modified by the wave packet. We measure the PL as a function of ∆t and the spatial coordinates of the laser spot parallel (the x-axis) and perpendicular (the y-axis) to the edge.

In this study, we focus on the ν = 1/3 fractional QH (FQH) state, which is one of the most fundamental Laughlin states [2], realized at a temperature of ∼40 mK, where the longitudinal resistance of our sample Rxx reaches approximately zero [See SM and Fig. S2(b)].

First, we present the time delay dependence of the PL spectra observed at fixed spatial points. The wave packet is excited by a square pulse of the duration τpulse [Fig. 2(a)]. When τpulse = 1 ns, the PL peak energy is blue-shifted at two time positions ∆t of ∼0 ns and ∼1 ns 17 μm (point 1 in Fig. S1 in SM) downstream from the excitation gate [Fig. 2(b)]. Herein, ∆t = 0 is defined by the moment of the first blue-shift. As τpulse is extended to 2 and 3 ns, the second blue-shift becomes delayed by the same amount [Figs. 2(c) and 2(d)], thus indicating that these shifts correspond to the fall and rise of the square pulse. Notably, no significant changes are observed in the PL spectra [Fig. 2(e)] 18 μm upstream from the excitation gate (point 2 in Fig. S1). Therefore, the stroboscopically observed changes in PL are induced by the electrically excited wave packet as it chirally propagates along the edge. The PL spectrum [Fig. 2(f)] observed at ∆t = −2 ns, observed before the first blue-shift, contains one intense peak; whereas the spectra during the blue shifts observed at ∆t = 0 and 3 ns appear to contain two peaks. The PL spectra at ν ≈ 1/3 may contain at most three peaks originating from the singlet and two triplet triplets [22]. These triplets, which can be classified as dark and bright triplets, are distinguished by their to-
The wave packet. During the rising part of the pulse, the PL spectrum appears as it did in the absence of the edge state, which is not excited during the flat part of the pulse, and is detected in the PL spectrum. Once the wave packet has not yet arrived at the focal point. The waveform of PL, excited by sawtooth pulses is analogous to \( \frac{dV_{ex}}{dt} \) [see Fig. S3(e)]. However, in the case of the square pulse [Fig. 2(a)], the response observed in the waveform of \( E_{PL} \) and \( I_{PL} \) [Figs. 2(f) and 2(g)] is significantly longer than the rise and fall times of \( V_{ex} \), which are ~100 ps. This may be because the lifetime of a trion is longer than the duration of the electronic disturbance caused by the wave packet (see SM).

Subsequently, we study the spatial domain. We first focus on the PL spectra at \( \Delta t = -2 \) ns, in which the wave packet has not yet arrived at the focal point. The I_{PL} waveform as a function of \( \Delta t \) near the sample edge is overall weaker than that of the QH bulk region [e.g. compare I_{PL} at \( y = 0.5 \) \( \mu m \) and \( y = 1 \) \( \mu m \) in Fig. 3(a)]. By moving the focal point towards the QH bulk region along the \( y \)-axis, \( I_{PL} \) is maximized at \( y \sim 1.25 \) \( \mu m \) before decreasing slightly [solid green line in Fig. 3(b)]. \( I_{PL} \) was previously shown to depend on \( B, \nu, \) spin polarization, and \( n_e \). Owing to the slope of the confining potential [Fig. 3(b) inset], \( n_e \) tends to decrease and then became zero beyond the sample edge (\( y < 0 \)), contributing to a decrease in \( I_{PL} \) leading to its eventual disappearance. In contrast, the PL peak energy \( E_{PL} \) tends to be constant in two regions, \( y < 1 \) \( \mu m \) and \( y > 3 \) \( \mu m \), and monotonically increases between these plateaux by ~0.8 meV. Among other factors, the photon energy of the PL is directly related to the bandgap [23, 27]. In the QH bulk region, the conduction and valence bands in the QW are flat in the \( xy \)-plane. Thus, \( E_{PL} \) is constant and independent of the spatial position except for small fluctuations owing to the intrinsic random potential on the QH edge states [26].

**FIG. 3.** (Color online) (a) \( \Delta t \) dependence of \( I_{PL} \) ingated between 1533.1 and 1536.5 meV at different values of \( y \). \( \tau_{pulse} \) is 1 ns. (b) Spatial dependence of \( I_{PL} \) and \( E_{PL} \) at three different values of \( \Delta t \). (Inset) Schematic of the band structure. The confinement potential \( U_e \) and \( U_h \) for the electrons and holes, respectively, are shown as a function of \( y \). (c) Spatial and temporal dependence of normalized integrated PL intensity \( I_{PL,N}(\Delta t, y) \) in \( y \) and \( \Delta t \). (see body text for definition.)
the order of $\sim 100 \mu eV$\cite{23}. Closer to the sample edge, the conduction and valence bands tend to shift upward owing to the pinning of the Fermi level by the surface state\cite{22} (see inset). Therefore, the $y$-component of the electric field $E_y = (dU_{eh})/dy$ drifts the electrons and holes toward the QH bulk and sample edge, respectively, and the effective bandgap decreases, resulting in a decrease in $E_{PL}$. The variation in $E_{PL}$ with $y$ suggests that the slopes of the conduction and valence bands gradually change in the region of $1.5 < y < 3 \mu m$. The fact that $E_{PL}$ is constant for $y < 1 \mu m$ can be attributed to the almost-constant slopes of the conduction and valence bands.

We consider the PL spectra when a wave packet reaches the focal point. $I_{PL}$ at $\Delta t = 0$ and 1 ns is weaker and stronger, respectively, than $I_{PL}$ at $\Delta t = -2$ ns where the wave packet has not yet arrived at the focal point [compare the red and blue solid lines with the green solid line in Fig. 3(b)]. In contrast, $E_{PL}$ responds to the wave packet differently depending on the $y$ position. $E_{PL}$ at $\Delta t = 1$ ns increases at $y < 1.75 \mu m$, whereas it decreases at $y > 1.75 \mu m$ [compare red and green dashed lines in Fig. 3(b)].

In Fig. 3(c), we plot the normalized $I_{PL}$ in the $y$-$\Delta t$ space defined as $I_{PL,N}(\Delta t, y) = \frac{I_{PL}(\Delta t, y)}{I_{PL,0}(y)}$, where $I_{PL,0}(y)$ denotes the averaged $I_{PL}$ in the range of $-2.3 < \Delta t < -1.2$ ns where the wave packet has not yet arrived at the focal point. Remarkably, the local minimum in $I_{PL,N}(\Delta t, y)$ extends several microns into the QH bulk [blue region in Fig. 3(c)] while curving toward a higher $\Delta t$. We observed similar curved features at two other locations relative to the excitation gate ($x = 10$ and $25 \mu m$, see SM and Fig. S4). We infer from the finite curvature that the local minimum of $I_{PL,N}$ penetrating as far as $y > 2.5 \mu m$ in the QH bulk is caused by the influence of the wave packet as it propagates at the edge while also emitting a disturbance directed toward the bulk with an average velocity in the $y$ direction of $v_y \sim 1 - 3 \times 10^4$ m/s. We attribute this disturbance to the magneto-roton collective excitations in the FQH bulk\cite{25}. The electrons with high energy propagate along the edge, emitting their energy to the bulk. This can excite the magneto-roton, i.e., the collective excitations of the incompressible bulk in the FQH regime\cite{25}. According to the magneto-roton theory\cite{25}, the collective excitation energy of the $\nu = 1/3$ Laughlin state is minimized at the wave number $k \sim 1/l_B$\cite{25}, where $l_B$ denotes the magnetic length. This is called the magneto-roton minimum, and is theoretically expected to be $\sim 0.1 \frac{eB}{h}$, where $\epsilon$ denotes the dielectric constant of GaAs. The velocity of the magneto-rotos $v_{MR}$ is obtained from their dispersion relation and is $\sim 2 \times 10^4$ m/s, which is an order of magnitude larger than $v_y$ obtained by our experiment. This difference can be partly attributed to the finite width of the QW, impurities, and mixing of higher Landau levels, which are known to reduce excitation energies. Because the excitation gap vanishes at the sample edge, further reduction is expected near the edge, wherein the influence of the edge state remains. Therefore, it is reasonable that $v_{MR}$ near the edge is considerably lower than that predicted in the ideal 2D system.

![Image](https://via.placeholder.com/150)

**FIG. 4.** (Color online) (a) Optical microscope image of the sample near the excitation gate. The $40 \times 29 \mu m^2$ image area is indicated by the dotted rectangle. (b)-(h) Normalized integrated PL intensity $I_{PL,N}$ map at $\nu = 1/3$ obtained at each $\Delta t$ at $B = 11.5$ T and 60 mK. (See body text for the definition of $I_{PL,N}$.) $\tau_{pulse}$ and the amplitude of $V_{ex}$ are, respectively, 0.5 ns and 0.3 V. One pixel is $1 \times 1 \mu m^2$. See also Movie S2 for the real-time video imaging of $I_{PL,N}$.

By raster-scanning the focal point both in the $x$ and $y$-directions and changing $\Delta t$, real-time video imaging of $I_{PL}$ can be obtained (Movie S1). To focus on the changes in $I_{PL}$ caused by $V_{ex}$, we extend the definition of $I_{PL,N}$ to the $x$-axis, i.e. $I_{PL,N}(\Delta t, x, y) = \frac{I_{PL}(\Delta t, x, y)}{I_{PL,0}(x, y)}$. Here, $I_{PL,0}(x, y)$ denotes averaged $I_{PL}$ in the rage of
−1.5 ≤ Δt ≤ −0.9 ns where the wave packet has not yet arrived at the focal point \((x, y)\). (See Movie S2 for the real-time video imaging of \(I_{\text{PL}, N}\) at \(\nu = 1/3\) and Fig. 4 for its temporal slices.) The \(I_{\text{PL}, N}\) in the downstream side of the sample edge is clearly decreased at \(\Delta t\) from 0.1 to 0.9 ns at \(\nu = 1/3\) [blue regions in Figs. 4(c)-4(f)]. This suggests that the excitation of \(\nu = 1/3\) edge propagates along the sample edge in accordance with the chirality. Notably, a decrease in \(I_{\text{PL}, N}\) (blue regions) is also observed around the excitation gate [Fig. 4(c)] and propagates toward the bulk region [Figs. 4(d)-4(f)]. From Figs. 4(c)-4(f), this extends to roughly \(\sim 5 - 10 \mu m\) for \(\sim 0.4 - 0.8\) ns; thus, the velocity of the wave is roughly estimated to be \(\sim 10^3 - 10^4\) m/s, which is faster than that observed near the edge \((y < \sim 4 \mu m)\) [Fig. 3(c)] and agrees with the theoretically expected \(v_{\text{MR}}\), suggesting that magneto-rotons are created by the excitation gate and propagate toward the bulk.

In summary, we reported on the excited state of the FQH edge and the bulk near the edge in real space and time using polarization-sensitive scanning stroboscopic confocal microscopy and spectroscopy. We observed the behavior of the wave packet propagating along the edge and the bulk region near the edge. The technique demonstrated is a powerful alternative to electrical transport measurements for investigating microscopic dynamical phenomena. It may be adapted to a wide range of other material systems because an optical response, such as reflection spectroscopy, is an alternative for detecting the electronic energy distribution in systems lacking PL.

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