Roomy: A System for Space Limited Computations

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Abstract
There are numerous examples of problems in symbolic algebra in which the required storage grows far beyond the limitations even of the distributed RAM of a cluster. Often this limitation determines how large a problem one can solve in practice. Roomy provides a minimally invasive system to modify the code for such a computation, in order to use the local disks of a cluster or a SAN as a transparent extension of RAM.

Roomy is implemented as a C/C++ library. It provides some simple data structures (arrays, unordered lists, and hash tables). Some typical programming constructs that one might employ in Roomy are: map, reduce, duplicate elimination, chain reduction, pair reduction, and breadth-first search. All aspects of parallelism and remote I/O are hidden within the Roomy library.

1 Introduction

This paper provides a brief introduction to Roomy [1], a new programming model and open source library for parallel disk-based computation. The primary purpose of Roomy is to solve space limited problems without significantly increasing hardware costs or radically altering existing algorithms and data structures.

Roomy uses disks as the main working memory of a computation, instead of RAM. These disks can be disks attached to a single shared-memory system, a storage area network (SAN), or the locally attached disks of a compute cluster. Particularly in the case of using the local disks of a cluster, disks are often underutilized and can provide several order of magnitude more working memory than RAM for essentially no extra cost.

There are two fundamental challenges in using disk-based storage as main memory:

**Bandwidth**: roughly, the bandwidth of a single disk is 50 times less than that of a single RAM subsystem (100 MB/s versus 5 GB/s). The solution is to use many disks in parallel, achieving an aggregate bandwidth comparable to RAM.

**Latency**: even worse than bandwidth, the latency of disk is many orders of magnitude worse than RAM. The solution is to avoid latency penalties by using streaming data access, instead of costly random access.

Roomy hides from the programmer both the complexity inherent in parallelism and the techniques needed to convert random access patterns into streaming access patterns. In doing so, the programming model presented to the user closely resembles that of traditional RAM-based serial computation.
The rest of this paper briefly describes the data structures provided by Roomy, and some example programming constructs that can be implemented using these data structures. Complete documentation, and instructions for obtaining the Roomy open source library, can be found on the Web at roomy.sourceforge.net.

## 2 Roomy Data Structures

Roomy data structures are transparently distributed across many disks, and the operations on these data structures are transparently parallelized across the many compute nodes of a cluster. Currently, there are three Roomy data structures:

- **RoomyArray**: a fixed size, indexed array of elements (elements can be as small as one bit).
- **RoomyHashTable**: a dynamically sized structure mapping keys to values.
- **RoomyList**: a dynamically sized, unordered list of elements.

There are two types of Roomy operations: delayed and immediate. If an operation requires random access, it is delayed. Otherwise, it is performed immediately. To initiate the processing of delayed operations for a given Roomy data structure, the programmer makes an explicit call to synchronize that data structure. By delaying random access operations they can be collected and performed more efficiently in batch.

Table 1 describes some of the basic Roomy operations. Some operations are specific to one type of Roomy data structure, while others apply to all three. The operations are also identified as either immediate (I) or delayed (D).

For performance reasons, it is often best to use a **RoomyArray** or **RoomyHashTable** instead of a **RoomyList**, where possible. Computations using **RoomyLists** are often dominated by the time to sort the list and any delayed operations. **RoomyArrays** and **RoomyHashTables** avoid sorting by organizing data into buckets, based on indices or keys.

## 3 Programming Constructs

Because Roomy provides data structures and operations similar to traditional programming models, many common programming constructs can be implemented in Roomy without significant modification. The one major difference is in the use of delayed random operations. To ensure efficient computation, it is important to maximize the number of delayed random operations issued before they are executed (by calling `sync` on the data structure).

Below are Roomy implementations of six programming constructs: map, reduce, set operations, chain reduction, pair reduction, and breadth-first search. Both map and reduce are primitive operations in Roomy. The others are built using Roomy primitives.
Table 1: Some basic Roomy operations. If an operation is specific to one type of data structure, it is listed under *RoomyArray*, *RoomyHashTable*, or *RoomyList*. Otherwise, it is listed as “common to all”. Also, the type of each operation is given as either immediate (I) or delayed (D).

| Data Structure  | Name    | Type | Description                                           |
|-----------------|---------|------|-------------------------------------------------------|
| RoomyArray      | access  | D    | apply a user-defined function to an element           |
|                 | update  | D    | update an element using a user-defined function       |
| RoomyHashTable  | insert  | D    | insert a given (key, value) pair in the table         |
|                 | remove  | D    | given a key, remove the corresponding (key, value) pair from the table |
|                 | access  | D    | given a key, apply a user-defined function to the corresponding value |
|                 | update  | D    | given a key, update a the corresponding value using a user-defined function |
| RoomyList       | add     | D    | add a single element to the list                      |
|                 | remove  | D    | remove all occurrences of a single element from the list |
|                 | addAll  | I    | adds all elements from one list to another           |
|                 | removeAll | I   | removes all elements in one list from another        |
|                 | removeDupes | I | removes duplicate elements from a list                |
| Common to all   | sync    | I    | process all outstanding delayed operations for the data structure |
|                 | size    | I    | returns the number of elements in the data structure  |
|                 | map     | I    | applies a user-defined function to each element       |
|                 | reduce  | I    | applies a user-defined function to each element and returns a value (e.g. the ten largest elements of the list) |
|                 | predicateCount | I | returns the number of elements that satisfy a given property (Note: this does not require a separate scan, the count is kept current as the data is modified) |
First, note that the code given here uses a simplified syntax. For example, the `doUpdate` method from the *chain reduction* programming construct below would be implemented in Roomy as:

```c
void doUpdate(uint64 localIndex, void* localVal, 
              void* remoteVal) {
    *(int*)localVal = 
    *(int*)localVal + *(int*)remoteVal;
}
```

The simplified version given here eliminates the type casting, and appears as:

```c
int doUpdate(int localIndex, int localVal, 
             int remoteVal) {
    return localVal + remoteVal;
}
```

A future C++ version of Roomy is planned that would use templates to make the simplified version legal code.

See the online Roomy documentation and API [1] for the exact syntax and function definitions.

**Map** The map operator applies a user-defined function to every element of a Roomy data structure. As an example, the following converts a RoomyArray into a RoomyHashTable, with array indices as keys and the associated elements as values.

```c
RoomyArray ra;  // elements of type T
RoomyHashTable rht;  // pairs of type (int, T)

// Function to map over RoomyArray ra.
void makePair(int i, T element) {
    RoomyHashTable_insert(rht, i, element);
}

// Perform map, then complete delayed inserts
RoomyArray_map(ra, makePair);
RoomyHashTable_sync(rht);
```

**Reduce** The reduce operator produces a result based on a combination of all elements in a data structure. It requires two user-defined functions. The first combines a partially computed result and an element of the list. The second combines two partially computed results. The order of reductions is not guaranteed. Hence, these functions must be associative and commutative, or else the result is undefined.

As an example, the following computes the sum of squares of the elements in a RoomyList.

```c
RoomyList rl;  // elements of type int

// Function to add square of an element to sum.
int mergeElt(int sum, int element) {
    return sum + element * element;
}

// Function to compute sum of two partial answers.
```
int mergeResults(int sum1, int sum2) {
    return sum1 + sum2;
}

int sum =
    RoomyList_reduce(rl, mergeElt, mergeResults);

The type of the result does not necessarily have to be the same as the type of the elements in
the list, as it is in this case. For example, the result could be the $k$ largest elements of the list.

**Set Operations** Roomy can support certain set operations through the use of a RoomyList. Some of these operations (particularly intersection) are sub-optimal when built using the current set of primitives. Future work is planned to add a native RoomySet data structure.

A RoomyList can be converted to a set by removing duplicates.

```c
RoomyList A; // can contain duplicate elements
RoomyList_removeDupes(A); // now a set
```

Performing set union, $A = A \cup B$, is also simple.

```c
RoomyList A, B;
RoomyList_addAll(A, B);
RoomyList_removeDupes(A);
```

Set difference, $A = A - B$, is performed by using just the `removeAll` operation, assuming $A$ and $B$ are already sets.

```c
RoomyList A, B;
RoomyList_removeAll(A, B);
```

Finally, set intersection is implemented as a union, followed set differences: $C = (A + B) - (A - B) - (B - A)$. Set intersection may become a Roomy primitive in the future.

```c
// input sets
RoomyList A, B;
// initially empty sets
RoomyList AandB, AminusB, BminusA, C;

// create three temporary sets
RoomyList_addAll(AandB, A);
RoomyList_addAll(AandB, B);
RoomyList_removeDupes(AandB);
RoomyList_addAll(AminusB, A);
RoomyList_removeAll(AminusB, B);
RoomyList_addAll(BminusA, B);
RoomyList_removeAll(BminusA, A);

// compute intersection
RoomyList_addAll(C, AandB);
RoomyList_removeAll(C, AminusB);
RoomyList_removeAll(C, BminusA);
```
**Chain Reduction**  Chain reduction combines each element in a sequence with the element after it. In this example, we compute the following function for an array of integers \(a\) of length \(N\)

\[
\text{for } i = 1 \text{ to } N-1 \\
a[i] = a[i] + a[i-1]
\]

where all array elements on the right-hand side are accessed before updating any array elements on the left-hand side.

In the following code, \(\text{val}_i\) represents \(a[i]\) and \(\text{val}_i\text{Minus1}\) represents \(a[i-1]\).

```java
RoomyArray ra; // array of ints, length N

// Function to complete updates
int doUpdate(int i, int val_i, int val_iMinus1) {
    return val_i + val_iMinus1;
}

// Function to be mapped over ra, issues updates
void callUpdate(int iMinus1, int val_iMinus1) {
    int i = iMinus1 + 1;
    if (i < N)
        RoomyArray update(ra, i, val_iMinus1, doUpdate);
}

RoomyArray map(ra, callUpdate); // issue updates
RoomyArray sync(ra); // complete updates
```

The computation is deterministic. The new array values will be based only on the old array values because Roomy guarantees that none of the delayed update operations will be executed until `sync` is called. The code above is implemented internally through a traditional scatter-gather operation.

**Parallel Prefix**  The chain reduction programming construct can also be used as the basis for a parallel prefix computation. At a high level, the parallel prefix computation is defined as

\[
\text{for } (k = 1; k < N; k = k \times 2)
\text{ if } i-k >= 0
\quad a[i] = a[i] + a[i-k];
\]

**Pair Reduction**  Pair reduction applies a function to each pair of elements in a collection. For an array \(a\) of length \(N\), pair reduction is defined as

\[
\text{for } i = 0 \text{ to } N-1
\for j = 0 \text{ to } N-1
f(a[i], a[j]);
\]

The following example inserts each pair of elements from a RoomyArray into a RoomyList. The variable `outerVal` represents \(a[i]\) and the variable `innerVal` represents \(a[j]\).
RoomyArray ra;  // array of int, length N
RoomyList rl;   // list containing Pair(int, int)

// Access function, adds a pair to the list
void doAccess(int innerIndex, int innerVal,
              int outerVal) {
    RoomyList_add(rl, new Pair(innerVal, outerVal));
}

// Map function, sends access to all other els
void callAccess(int outerIndex, int outerVal) {
    for (innerIndex = 0 to N-1
         RoomyArray_access(ra, innerIndex, outerVal, doAccess);
    }
RoomyArray_map(ra, callAccess);
RoomyArray_sync(ra);  // perform delayed accesses
RoomyList_sync(rl);   // perform delayed adds

One can think of the RoomyArray_map method as the outer loop, the callAccess method as
the inner loop, and the doAccess method as the function being applied to each pair of elements.

**Breadth-first Search**  Breadth-first search enumerates all of the elements of a graph, exploring
elements closer to the starting point first. In this case, the graph is implicit, defined by a starting
element and a generating function that returns the neighbors of a given element.

// Lists for all els, current, and next level
RoomyList* all = RoomyList_make("allL", eltSize);
RoomyList* cur = RoomyList_make("lev0", eltSize);
RoomyList* next = RoomyList_make("lev1", eltSize);

// Function to produce next level from current
void genNext(T elt) {
    /* User-defined code to compute neighbors ... */
    for (nbr in neighbors
         RoomyList_add(next, nbr);
    }

// Add start element
RoomyList_add(all, startElt);
RoomyList_add(cur, startElt);

// Generate levels until no new states are found
while (RoomyList_size(cur)) {
    // generate next level from current
    RoomyList_map(cur, genNext);
    RoomyList_sync(next);

    // detect duplicates within next level
}
One of the initial tests of Roomy was to use breadth-first search to solve the \textit{pancake sorting problem}. Pancake sorting operates using a sequence of prefix reversals (reversing the order of the first \(k\) elements of the sequence). The sequence can be thought of as a stack of pancakes of varying sizes, with the prefix reversal corresponding to flipping the top \(k\) pancakes. The goal of the computation is to determine the number of reversals required to sort any sequence of length \(n\).

Using Roomy, the entire application took less than one day of programming and less than 200 lines of code. Breadth-first search was implemented using a \texttt{RoomyArray}, similar to the \texttt{RoomyList}-based version presented above.

Three different solutions to the pancake sorting problem, each using one of the three Roomy data structures, is available in the Roomy online documentation [1].

\section*{4 Acknowledgments}

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\section*{References}

[1] Daniel Kunkle. Roomy: A C/C++ library for parallel disk-based computation, 2010. \url{http://roomy.sourceforge.net/}. 

```c
RoomyList_removeDupes(next);

// detect duplicates from previous levels
RoomyList_removeAll(next, all);

// record new elements
RoomyList_addAll(all, next);

// rotate levels
RoomyList_destroy(cur);
cur = next;
next = RoomyList_make(levName, eltSize);
```