The photonic spin Hall effect (SHE) is generally believed to be a result of an effective spin-orbit coupling, which describes the mutual influence of the spin (polarization) and the trajectory of the light beam. The photonic SHE holds great potential for precision metrology owing to the fact that the spin-dependent splitting in photonic SHE are sensitive to the physical parameter variations of different systems. Remarkably, using the weak measurements, this tiny spin-dependent shifts can be detected with the desirable accuracy so that the corresponding physical parameters can be determined. Here, we will review some of our works on using photonic SHE for precision metrology, such as measuring the thickness of nanometal film, identifying the graphene layers, detecting the strength of axion coupling in topological insulators, and determining the magneto-optical constant of magnetic film.

Keywords: photonic spin Hall effect, spin-orbit coupling, weak measurements

1. INTRODUCTION

The photonic spin Hall effect (SHE) manifests itself as spin-dependent splitting of left- and right-handed circularly polarized components when a spatially confined light beam is reflected or transmitted at an interface. The photonic SHE can be regarded as a direct optical analogy of SHE in an electronic system, in which the spin photons play the role of the spin charges and a refractive index gradient plays the role of the applied electric field. This interesting phenomenon is generally believed to be a result of an effective spin-orbit coupling, which describes the mutual influence of the spin (polarization) and the trajectory of the light beam. There are two types of geometric phases playing the important role in photonic SHE: the spin redirection Berry phase and the Pancharatnam-Berry phase. The photonic SHE is currently attracting growing attention and has been intensively investigated in different physical systems such as optical physics, high-energy physics, semiconductor physics, and plasmonics. Remarkably, the spin-dependent splitting in photonic SHE are sensitive to the physical parameter variations of different systems, and therefore it holds great potential applications in precision metrology. However, the spin-dependent splitting of photonic SHE in these systems is just a few tens of nanometers so that the actual equipment can not distinguish it directly. We resolve this problem by using the precise signal enhancement technique called quantum weak measurements which has attracted a lot of attention. The idea of weak measurements can be described as follows: if we initially select the quantum system with a well-defined preselection state, the corresponding large expectation values can be obtained with a suitable postselection state, which makes the eigenvalues to be clearly distinguished. Using the quantum weak measurement, the photonic SHE can be detected with the desirable accuracy.

In this paper, we will review some of our recent works on using photonic SHE for precision metrology, such as measuring the thickness of nanometal film, identifying the graphene layers, detecting the strength of axion coupling in topological insulators, and determining the magneto-optical constant of magnetic film. We find that the physical parameter variations in these systems can effectively change the spin-dependent displacements. We firstly establish the quantitative relationship between the spin-dependent shifts and the physical parameters. After detecting the spin-dependent displacements with weak measurement method, we can accurately determine
The sample can be nanometal film, graphene film, topological insulators, and magnetic film. A linearly polarized beam reflects on the sample and then splits into left- and right-handed circularly polarized components, respectively. $\delta_{(+)r}$ and $\delta_{(-)r}$ denote the in-plane shift of left- and right-handed circularly polarized components. $\delta_{(+)}^y$ and $\delta_{(-)}^y$ denote the transverse spin-dependent displacements. Here, $\theta_i$ is the incident angle.

The rest of the paper is organized as follows. In Sec. 2, we establish a general propagation model to describe the photonic SHE on the sample. In the Sec. 3, we firstly introduce the weak measurements experimental process. Then, we will briefly review our recent works on using photonic SHE for precision metrology. Finally, a conclusion is given in Sec. 4.

**2. GENERAL PROPAGATION MODEL**

Figure 1 schematically draws the photonic SHE of light beam reflection from a sample interface. We firstly establish the quantitative relationship between the spin-dependent shifts in photonic SHE and the physical parameters of sample. Here, the physical parameters include the thickness of nanometal film, graphene’s layers, axion angle in topological insulators, and the magneto-optical constant of magnetic film. The incident polarization states are chosen as $|H\rangle$ and $|V\rangle$. In the spin basis, the horizontal and vertical polarization states can be expressed as $|H\rangle = (|+\rangle + |-\rangle)/\sqrt{2}$ and $|V\rangle = i(|-\rangle - |+\rangle)/\sqrt{2}$. Corresponding, the states of reflected beam can be obtained:

$$|H\rangle \rightarrow \frac{r_p}{\sqrt{2}} \left[ \exp(+ik_{ry}\delta_{(+)r}^H)|+\rangle + \exp(-ik_{ry}\delta_{(+)r}^H)|-\rangle \right],$$

$$|V\rangle \rightarrow \frac{ir_s}{\sqrt{2}} \left[ -\exp(+ik_{ry}\delta_{(+)}^V)|+\rangle + \exp(-ik_{ry}\delta_{(+)}^V)|-\rangle \right].$$

In the above equations, $\delta_{(+)}^H = (1 + r_s/r_p) \cot \theta_i/k_0$, $\delta_{(+)}^V = (-1 - r_p/r_s) \cot \theta_i/k_0$. We should note that, as for the topological insulators, the states of reflected beam have different forms. The detailed discussions can be found in our previous work.

The photonic SHE manifests for the spin-dependent splitting of left- and right-handed circularly polarized components. We consider the spin separation in the x direction (in-plane shift) and y direction (transverse shift). In the following, we calculate the shifts of these two spin components. The wavefunction of reflected photons is composed of the packet spatial extent $\phi(k_{ry})$ and the polarization description $|H, V\rangle$:

$$|\Phi^{H,V}\rangle = \int dk_{ry} \phi(k_{ry})|k_{ry}\rangle|H, V\rangle.$$  

After photons reflection from the sample interface, the initial state $|\Phi_{initial}^{H,V}\rangle$ evolve into the final state $|\Phi_{final}^{H,V}\rangle$. As a result of spin-orbit coupling, the shifts of the two spin components compared to the geometrical-optics
Figure 2. The experimental setup in weak measurements. The sample is a BK7 prism prepared with the nanometal film, graphene film, topological insulators, and magnetic film. L1 and L2, lenses with effective focal length 50mm and 250mm, respectively. HWP, half-wave plate (for adjusting the intensity). P1 and P2, Glan Laser polarizers. CCD, charge-coupled device (Coherent LaserCam HR). The light source is a 21mW linearly polarized He-Ne laser at 632.8nm (Thorlabs HNL210L-EC). The inset shows the states of preselction and postselection. Here, the preselection state is prepared in $|V\rangle$.

prediction are given by

$$\delta_{H,V}^{H,V} = \frac{\langle \Phi_{H,V} | i\partial_{k_{\perp}} | \Phi_{H,V} \rangle}{\langle \Phi_{H,V} | \Phi_{H,V} \rangle}.$$  \hspace{1cm} (4)

Here, we suppose the $\phi(k_{xy})$ is a Gaussian wave function. Calculating the reflected shifts of photonic SHE requires the explicit solution of the boundary conditions at the sample interfaces. As for the nanometal film and graphene film, we need to deal with the multilayer structure model. Thus, we need to know the generalized Fresnel reflection of the sample,

$$r_A = \frac{R_A + R_A' \exp(2ik_0\sqrt{n^2 - \sin^2 \theta_i}d)}{1 + R_A R_A' \exp(2ik_0\sqrt{n^2 - \sin^2 \theta_i}d)}.$$  \hspace{1cm} (5)

Here, $A \in \{p, s\}$, $R_A$ and $R_A'$ is the Fresnel reflection coefficients at the first interface and second interface, respectively. $n$ and $d$ represent the refractive index and the thickness of the nanometal film and graphene film, respectively.

3. PHOTONIC SPIN HALL EFFECT FOR PRECISION METROLOGY

We have established the relationship between the physical parameters of sample and the spin-dependent displacements induced by photonic SHE. Next, we will use the weak measurements method to detect the tiny shifts. After detecting the spin-dependent displacements, we can accurately determine these physical parameters. As shown in Fig. 2, our experimental setup is similar to that in Ref\(^{36}\). Our samples are the usual BK7 prism prepared with the nanometal film, graphene film, topological insulators, and magnetic film. A Gauss beam generated by He-Ne laser is firstly focused by the lens (L1) and experiences preselection in the state $|\psi_1\rangle = |H\rangle$ or $|V\rangle$ with the polarizer P1. When the light beam reflects from the sample interface, the photonic SHE happens allowing for the left- and right-handed circularly polarized components splitting in the x and y directions corresponding to the in-plane and transverse displacements. This process can be seen as the weak interaction allowing for the coupling between the observable and the meter. And then the beam passes through the second polarizer P2 preparing for the postselection state $|\psi_2\rangle = |V \pm \Delta\rangle$ or $|H \pm \Delta\rangle$. At the surface of the second polarizer, the two spin components experience destructive interference making the enhanced shift in the meter much larger than the initial one. Calculating the reflected field distribution yields the amplified shifts of photonic SHE. After
passing through the second lens (L2), a CCD is used to capture the optical signal and measure the amplified shifts. The process discussed above is called the weak value amplification and $\Delta$ is the postselection angle. We should note that the imaginary weak value also corresponds to a shift of the meter in momentum space, which leads to the possibility of even larger enhancements following the beam free evolution. This process can be seen as propagation amplification that produces the amplified factor $F$. In the following, we will review some of our recent works on using photonic SHE for precision metrology.

In the first work, we have used the photonic SHE to measure the thickness of nanometal film. We establish a general propagation model to describe the photonic SHE on a nanometal film and reveal the impact of the corresponding physical parameters on the spin-dependent splitting in photonic SHE. It is well known that the photonic SHE manifests itself as the spin-orbit coupling. We find that the spin-orbit coupling in the photonic SHE can be effectively modulated by adjusting the thickness of the metal film. A similar effect can also be observed in layered nanostructures, in which the transverse displacement changes periodically with the air gap increasing or decreasing. Additionally, the transverse displacement is sensitive to the thickness of metal film in certain range for horizontal polarization light beam. We also note that a large negative transverse shift can be observed.

Next, we focus our attention on the weak measurements experiment. Here, the BK7 glass substrate coated Ag film is chosen as our sample (with three different thickness 10nm, 30nm and 60nm). The experimental setup is described in the above contents. We measure the displacements of photonic SHE on the nanometal film every $5^\circ$ from $30^\circ$ to $85^\circ$ in the case of horizontal and vertical polarization, respectively. Limited by the large holders of the lens, polarizers and He-Ne laser, displacements at small incident angles were not measured. It should be noted that the experimental results are in good agreement with the theoretical ones when the film thicknesses
Figure 4. Experimental results for determining the layer numbers of graphene. (a) shows the theoretical spin-dependent shifts in the case of graphene layer numbers changing from one to five. (b) describes the experimental results for determining the layer numbers of graphene. The lines represent the theoretical results. The circle, square and triangle show the experimental data obtained from three different areas of the graphene sample. (c) Raman spectroscopy of the sample. The inset shows the graphene sample.

are 30nm and 60nm. However, we observe a small deviation when the thickness is 10nm. Note that the thickness of the nanometal film has an error limited by the experimental condition. When the thickness reaches to 10nm, the SHE of light is very sensitive to the error. It is the reason why there is a small deviation between the experimental and the theoretical data. From the experimental results, we can conclude that the actual thickness of the film is about 12nm (Fig. 3). These findings provide a pathway for modulating the photonic SHE and thereby open the possibility of developing nanophotonic applications.

We also propose using the photonic SHE to identify the graphene layers. The quick and convenient technique for identifying the layer numbers of graphene film is important for accelerating the study and exploration of graphene material. There are many methods for determining the layer numbers of graphene film, yet existing limitation. For example, atomic force microscopy technique is the straight way to determine the layer numbers of graphene. But this method shows a slow throughput and may induce damage to the sample. Unconventional quantum Hall effects are usually used to distinguish one layer and two layers graphene from multiple layers. Raman spectroscopy shows characteristic for quick and nondestructive measuring the layer numbers of graphene. However, it is not obvious to tell the differences between bilayer and a few layers of graphene films. We find that the photonic SHE can serve as a useful metrological tool for characterizing the structure parameters’ variations of nanostructure due to their sensitive dependence. So, the photonic SHE may have a potential to determine the layer numbers of graphene.

We establish the relationship between the spin-dependent displacements and the graphene layer numbers. The weak measurements method has been used to detect the transverse shifts, and so the graphene layer numbers can be obtained. However, there exists two unknown parameters (refractive index and layer numbers of graphene) to be identified. Before identifying the graphene layers, we need to choose the suitable refractive index parameter of graphene. We choose one suitable refractive index according from the work of Bruna and Borini. Here, the refractive index of graphene is about $n=3.0 + 1.149i$ at 633 nm. Through measuring the spin-dependent shifts of photonic SHE on the graphene film, we prove that this refractive index is suitable for actual situation. Using the suitable refractive index $n=3.0 + 1.149i$ at 633 nm, we can identify the layer numbers of an unknown graphene film. It should be noted that we cannot fabricate the graphene film with the precise layer numbers when the graphene film has more than two layers. We just know the approximate layer numbers ranging from three to five layers. We want to determine the actual layer numbers of this graphene film. As shown in Fig. 4 we measure the transverse displacements with the incident angle changing from 56° to 62°. To avoid the influence of impurities and other surface quality factors of graphene film, we carried out the experiments for three different areas of the graphene sample. It is concluded that the actual layer numbers of the film is three.

Recently, the topological insulators (TIs) material has aroused tremendous interest. It has gapless helical surface states owing to the topological protection of the time-reversal symmetry and represents a full energy gap in the bulk. In a recent paper, we theoretically investigate the photonic SHE of a Gaussian beam reflected
Figure 5. The photonic SHE and magneto-optical Kerr effect induced by axion coupling at air-TI interfaces in the case of horizontal polarization (a-d) and the corresponding weak measurements (e). Here the parameters are the refractive index of TIs $n=10$ (appropriate for the TIs such as $Bi_{1-x}Se_x$). The beam waist is selected as $w_0 = 20\lambda$. In the weak measurements process, the incident angle is chosen as $\theta_i = 84^{\circ}$.
Figure 6. The preliminary results for determining the magneto-optical constants. (a) and (b) describe the initial spin-dependent shifts of Fe and Co materials in the case of H and V polarizations. The corresponding amplified displacements under the condition of H and V polarizations are shown in (c) and (d).

We reveal that the spin-orbit coupling effect in TIs can be routed by adjusting the axion angle variations. It is shown that the magneto-optical Kerr effect can be significantly altered due to the axion coupling and shows close relationship with spin-dependent splitting in photonic SHE [Fig. 5(a) and 5(b)]. We find that, unlike the transverse spin-dependent splitting, the in-plane one is sensitive to the axion angle [Fig. 5(c) and 5(d)]. Due to the limitation of experimental condition, we theoretically propose a weak measurement method to determine the strength of axion coupling by probing the in-plane splitting of the photonic SHE.

The incident beam is focused by the lens and is preselected in the horizontal polarization, and then it is postselected in the polarization state with \( |V\pm\Delta\rangle \) (\( \Delta \) is the amplified angle). The relevant amplitude of the reflected field at a plane can be obtained, allowing for calculation of amplified displacement. The theoretical amplified shifts are shown in Fig. 3(e). Here the incident angle is fixed to 84°. Then we obtain the amplified displacements varying with axion angle and amplified angle. For a fixed angle \( \Delta \), the amplified in-plane shifts change clearly with the different axion angles, and so we can measure the axion coupling effect by determining the in-plane displacements with weak measurements. These findings offer us potential methods for determining the strength of the axion coupling and provide new insight into the interaction of light with TIs.

We have also used the photonic SHE for determining the magneto-optical constant of magnetic film and the preliminary results can be seen in Fig. 6. The magneto-optical constant is an important parameter for the study and exploration of magnetic material. The relationship between the spin-dependent splitting in photonic SHE and the magneto-optical constant of magnetic film is established. Here, we choose the Fe and Co as our samples, which have different magneto-optical constants \( Q_{Fe} = 0.0215 - 0.001645 \) and \( Q_{Co} = 0.0189 - 0.0043 \) at 633 nm. From the Fig. 6(a) and 6(b), we can see that the spin-dependent displacements are sensitive to the magneto-optical constants of different magnetic materials. So, we can determine the magneto-optical constants by measuring the spin-dependent splitting of photonic SHE. In our experiment, the weak measurements has been used to detect this tiny shifts [the preliminary theoretical results are shown in Fig. 6(c) and 6(d)]. We also find that the amplified spin shifts are sensitive to the variations of magneto-optical constants (Fe and Co). Importantly, the Kerr rotation angle in magneto-optical Kerr effect can also be detected by using this way, which shows higher accuracy than the normal extinction method. In fact, our experiment is in progress and the
4. CONCLUSIONS

In summary, we have reviewed our recent works on using photonic SHE for precision metrology. After establishing the quantitative relationship between the spin-dependent shifts in photonic SHE and the physical parameters in different systems, we have used the weak measurements methods for measuring the thickness of nanometal film, identifying the graphene layers, detecting the strength of axion coupling in topological insulators, and determining the magneto-optical constant of magnetic film. These findings provide a practical application for photonic SHE and thereby open the possibility of developing spin-based nanophotonic device.

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