New Insights From Long-Term Measurements of Inner Belt Protons (10s of MeV) by SAMPEX, POES, Van Allen Probes, and Simulation Results

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Abstract The Solar, Anomalous, and Magnetospheric Particle Explorer (SAMPEX) mission provided long-term measurements of 10s of megaelectron volt (MeV) inner belt (L < 2) protons (1992–2009) as did the Polar-orbiting Operational Environmental Satellite-18 (POES-18, 2005 to present). These long-term measurements at low-Earth orbit (LEO) showed clear solar cycle variations which anticorrelate with sunspot number. However, the magnitude of the variation is much greater than the solar cycle variation of galactic cosmic rays (>GeV) that are regarded as a source of these trapped protons. Furthermore, the proton fluxes and their variations sensitively depend on the altitude above the South Atlantic Anomaly (SAA) region. With respect to protons (>36 MeV) mirroring near the magnetic equator, both POES measurements and simulations show no obvious solar cycle variations at L > 1.2. This is also confirmed by recent measurements from the Van Allen Probes (2012–2019), but there are clear solar cycle variations and a strong spatial gradient of the proton flux below L = 1.2. A direct comparison between measurements and simulations leads to the conclusion that energy loss of trapped protons due to collisions with free and bound electrons in the ionosphere and atmosphere is the dominant mechanism for the strong spatial gradient and solar cycle variation of the inner belt protons. This fact is also key of importance for spacecraft and instrument design and operation in near-Earth space.

1. Introduction

Interplanetary space is permeated by galactic cosmic rays (GCRs), mostly protons with kinetic energies above hundreds of megaelectron volts (MeV). Most of these particles are likely produced by supernovae in our galaxy (e.g., Blasi, 2013). Soon after the discovery of Earth’s Van Allen radiation belts six decades ago, it was recognized that the main source of inner belt (L < 2) protons, with kinetic energies of 10s of MeV to gigaelectron volt (GeV), is Cosmic Ray Albedo Neutron Decay (CRAND) (e.g., Dragt et al., 1966; Singer, 1958). In this process, cosmic rays (>GeV energies) interact with neutral atoms in the upper atmosphere to produce energetic albedo neutrons which decay into protons, electrons, and antineutrinos. Most of the kinetic energy is retained by the protons, and some of these consequently become geomagnetically trapped in the inner belt region.

Ground neutron monitor (NM) measurements, used to infer cosmic ray intensity variations even before the space age (e.g., Simpson, 2000), exhibit a strong geomagnetic latitude dependence. NMs at different geomagnetic latitudes have different cutoff energies for incoming cosmic rays, from 100s of MeV in the polar region to multi-GeV in the inner belt (L < 2, corresponding to geomagnetic latitude of <45°) (e.g., Selesnick et al., 2007; Smart & Shea, 2005). All NM data show a variation in cosmic rays on the 11-year sunspot cycle and the 22-year solar magnetic cycle. Occasionally, the Sun emits energetic particles (mostly protons) of sufficient energy and intensity to be significantly above the cosmic ray level. They are detected by NMs at high latitudes as well. Such episodic events, ranging from a few times in a year to a few times in a sunspot cycle, are termed “ground-level enhancements” (GLEs) (e.g., Poluianov et al., 2017; Simpson, 1990).

Solar energetic protons are another source of 10s of MeV protons trapped in the inner belt but from a different process: inward radial diffusion of pretrapped energetic protons at larger L (e.g., Selesnick et al., 2007).
During solar energetic particle (SEP) events, some protons can become trapped in the Earth’s magnetosphere (e.g., Hudson et al., 1995; Looper et al., 2005; Lorentzen et al., 2002) and diffuse inward to \( L < 2 \), adding to the pre-existing trapped protons in the inner belt (Selesnick et al., 2014, 2016, 2018). The initial trapping process is understood, in principal, to be due to electric and magnetic field fluctuations affecting Störmer orbits (Störmer, 1955). Solar protons are more likely to become trapped deep inside Earth’s magnetosphere if followed by a large interplanetary shock impact (Blake et al., 1992; Hudson et al., 1995). Efforts have been made to understand the initial entrance of solar energetic protons to different geomagnetic latitudes (cutoff) (e.g., Engel et al., 2016; Kress et al., 2004, 2010; Leske et al., 2001; Qin et al., 2019). Nonetheless, it is still uncertain how many solar protons can become trapped in the magnetosphere for a given SEP event (Selesnick et al., 2010). It was also recognized that the SEP contribution to trapped protons inside \( L < 1.3 \) through radial diffusion is insignificant (e.g., Jentsch, 1981; Selesnick & Albert, 2019).

Over the last four decades, Voyager 1 (V1) and Voyager 2 (V2), launched in 1977–1978 (https://voyager.jpl.nasa.gov/mission/status/), have been measuring cosmic rays in the heliosphere and beyond (e.g., Cummings et al., 2016). Figure 1 shows the long-term flux of energetic particles from the Cosmic Ray Subsystem (CRS) instrument (Stone et al., 1977) onboard V1 and V2 as they traveled from the inner heliosphere to the outer heliosphere and into the local interstellar medium. The top two panels show the differential flux of \( \sim 270-350 \) MeV/nuclei (mostly protons) measured by V1 and V2. The solar cycle variation of the cosmic rays is clear, almost in phase with the Thule NM measurement (second from last panel), particularly when V1 and V2 are not too far from the Earth, and in anticorrelation with the sunspot number (last panel). The solar cycle modulation of cosmic ray intensity was stronger in the inner heliosphere and got weaker as V1 and V2 traveled to the outer heliosphere. After they exited the heliosphere into the local interstellar medium, the solar cycle modulation virtually disappeared (more apparent on V1). Incoming cosmic rays are modulated by the solar wind, especially by stronger solar magnetic structures during solar maximum (e.g., Cane et al., 1999). The solar cycle modulation depends on the particles’ energy and is greater for the lower energy particles (e.g., Usoskin et al., 2005).

In the rest of this paper, we focus on the characteristics of trapped inner belt protons (10s of MeV) based on long-term measurements from Solar, Anomalous, and Magnetospheric Particle Explorer (SAMPEX), Polar-orbiting Operational Environmental Satellite (POES), Van Allen Probes, and model simulations. We will show that the solar cycle variation of inner belt protons measured by low-Earth orbit (LEO) satellites is mainly due to losses from atmospheric collisions and that the inner belt proton intensity and solar cycle variation measured at LEO depend sensitively on altitude and thus the particle’s pitch angle. Detailed comparison between POES measurements and model simulations for the protons mirroring near the magnetic equator shows a strong gradient in the proton flux. Its solar cycle variation is only obvious at \( L < 1.2 \), which is also confirmed by recent measurements from the Van Allen Probes (2012–2019) in geo-transfer-like orbit. It is remarkable that the general model simulations, in which the decay of the proton fluxes is mainly due to energy loss to free and bound electrons in the local plasma and neutral atmosphere and is solar cycle dependent (Selesnick & Albert, 2019), reproduce the measurement well. This leads to a consolidated understanding that the solar cycle variation of the ionospheric and atmospheric density dominates the observed solar cycle variation of trapped inner belt proton flux.

2. Observations and Discussions

2.1. SAMPEX Measurements

The SAMPEX mission was launched into a \( \sim 510 \) km \( \times \) \( 690 \) km altitude and \( 82^\circ \) inclination orbit in July of 1992. The altitude of SAMPEX decayed slowly for the first 8 years and faster afterwards, reaching \( 410 \times 500 \) km by 2008; it re-entered the atmosphere on 13 November 2012 (Baker, Mazur, & Mason, 2012). In order to show the long-term variation of energetic protons at a given altitude, we plot the differential flux of 27.4- to 37.4-MeV protons measured by SAMPEX/PET (Cook et al., 1993) from late 1992 to late 2009 (when PET ceased operation) at an altitude around 500 km (\( \pm 20 \) km) and \( L = 1.33-1.42 \) in the top panel of Figure 2. Also plotted in Figure 2 are the “Delaware” NM (\( L = 2.4 \)) measurements and the sunspot number. The solar cycle variation is obvious in the proton flux and the NM measurements created by GCR that reach the atmosphere at this magnetic latitude (50°, \( L = 2.4 \)). However, the magnitude...
of the variation is vastly different. For a GCR proton to reach the atmosphere in $L < 1.42$ (corresponding to a magnetic latitude of 33°) and $L = 2.4$, it would need to have an energy of $>6$ and $\geq 2.3$ GeV, respectively (Selesnick et al., 2007; Smart & Shea, 2005). The modulation by the solar wind of multi-GeV GCR is limited, as shown by the relative variation of about 20% ($[\text{flux}_{\text{max}} - \text{flux}_{\text{min}}] / \text{flux}_{\text{min}}$) of the NM measurement (Panel 2) over a solar cycle (the relative variation of the NM at Mexico City, $L \sim 1.3$, is about 14.8%). However, the relative solar cycle variation of the satellite-measured proton flux (Panel 1) is about 300%, which suggests that the solar cycle variation of trapped inner belt protons is not due to this source. It was recognized earlier that the solar cycle variation of the upper atmosphere and ionosphere significantly influences low-altitude energetic protons (e.g., Huston & Pfitzer, 1998; Miyoshi et al., 2000; Qin et al., 2014). It is good to consolidate this understanding by comparing the trapped proton measurements with ground NM measurements at different latitudes and direct GCR measurements in the interplanetary space, although the 100s of MeV protons shown in Figure 1 can barely reach the atmosphere at the high latitudes ($>60°$) and even a higher rigidity (or energy) is required to reach the atmosphere at lower latitudes (e.g., Selesnick et al., 2007; Smart & Shea, 2005).
If we approximate the solar cycle variations of the measured proton flux (top panel of Figure 2) and sunspot number (bottom panel of Figure 2) by sine curves (dashed green lines) with an 11-year period, we can estimate that there exists a phase lag of 154 days between the sunspot number and the proton flux. This phase lag can be understood as how fast the trapped proton flux, which enhanced during solar min, decayed when the ionospheric and atmospheric densities increased during solar max. Obviously, the estimate of this phase lag has its uncertainty, and also this phase lag should be dependent on the altitude of measurements of the protons flux. Both aspects will be discussed next subsection.

2.2. POES Measurements

In comparison, we analyzed the long-term measurements from POES-18, which was launched on 20 May 2005, into a Sun-synchronous orbit (99.2° inclination) with an 848 km x 869 km altitude (Sandanger et al., 2015). There are only integral fluxes available before 2015 (Evans & Greer, 2004; https://satdat.ngdc.noaa.gov/sem/poes/data/). To plot the long-term measurements, we merged the integral flux (before 2015) and the differential flux (after 2015), displayed in top two panels in Figure 3. Sunspot number and $F_{10.7}$ measurements (both daily averaged) are plotted in the bottom two panels. The solar cycle variation of the energetic proton flux is still obvious, but the relative variation of the proton flux, $(\text{flux}_{\text{max}} - \text{flux}_{\text{min}})/\text{flux}_{\text{min}}$, at these higher altitudes is much smaller than the SAMPEX/PET measurements at lower altitudes.
altitudes. The relative solar cycle variation is only about 21% for both >36- and >140-MeV protons, which suggests that loss from atmospheric collision is much smaller at this higher altitude.

If we approximate the solar cycle variations of the measured proton flux (Figure 3a) and sunspot numbers (Figure 3c) by sine curves with an 11-year period, we can estimate that there exists a phase lag of 730 days, which is much longer than the phase lag between the SAMPEX proton flux and the sunspot numbers. This much greater phase lag is consistent with the much smaller solar cycle variations exhibited by the POES measurements, which were taken at higher altitude (~860 km), where the influence of ionosphere and atmosphere is much weaker than at ~500 km and thus the residence time of the protons measured at ~860 km is much longer.

We also did the phase lag calculation for the >140-MeV protons (Figure 3b) in the same manner and found the same results as for >36-MeV protons. We would expect that there should be a longer phase lag for higher energy protons since they are less likely to be affected by the atmospheric density. However, we should also realize that the sine fitting is an approximate method, which has an uncertainty of 1 year (one grid of the points used for the fitting). Another point should be mentioned here is that the relative variations of the proton flux for these two panels over a solar cycle are about the same as well (~21%).

It is worth pointing out that the small periodic variation (~120-day periodicity) in the Figures 3a and 3b is associated with the precession of the orbit, with the peaks corresponding to apogee (869 km) in the Southern Hemisphere and above South Atlantic Anomaly (SAA) and the dips corresponding to perigee (848 km) in the Southern Hemisphere. The relative variation is 2.9% for >36-MeV protons and 2.7% for >140-MeV protons, even though the altitude difference is only 21 km. This detailed feature suggests that trapped inner belt protons have a strong altitude gradient, confirming early results (e.g., Parsignault et al., 1981). This spatial gradient also suggests that there would be an east-west asymmetry if measured by a unidirectional detector as the eastward traveling fluxes, whose guiding centers are at higher altitudes, are expected to be greater than the westward traveling fluxes, whose guiding centers are at lower altitudes because of the finite protons gyroradii (Heckman & Nakano, 1963; Lenchek & Singer, 1962). For example, the averaged flux for >36-MeV protons has a relative increase of 2.9% from 848 to 869 km above SAA \( J_{869} = J_{848} \exp \left[ -21/h \right] \); \( J_{869} / J_{848} = 0.029 \). This gives the average scaleheight (h) of the proton flux around this region as ~735 km, which is far greater the gyroradius of a 36-MeV proton at this location.

![Figure 3. 30-day averaged proton flux at L = 1.33–1.42 during June 2015 to December 2018 measured by NOAA POES-18 satellite are plotted in Panel (a) (>36-MeV proton flux) and Panel (b) (>140-MeV proton flux); Panel (c) is the sunspot number; Panel (d) is the F10.7 solar index. Note that after 2014, there is no integral energy channel of proton flux in data product (https://satdat.ngdc.noaa.gov/sem/poes/data/; Evans & Greer, 2000). Thus, two nearby differential energy channels (25 and 100 MeV) of proton fluxes are presented on the right of this figure. The sunspot number and F10.7 solar indices are from OMNIWeb (http://spdf.gsfc.nasa.gov/pub/data/omni/). The L is directly obtained from the POES data product, which uses a current IGRF model for the epoch midway through the year the data were acquired. The magnetic calculations are updated once a year using the new IGRF model and satellite orbit information. The dashed blue curves on Panels a–c are fitted sine curves with an 11-year period.](image-url)
The eastward traveling flux would be ~15% higher than the westward traveling flux if measured by a unidirectional detector at this location. However, the proton detectors on POES have a large field of view (FOV), 120° and 180° for >36 and >140 MeV, and the detectors are pointing toward the zenith directions. So the east-west asymmetry will not be significant from these detectors’ measurements. In addition, we have averaged the measurements during their descending and ascending phases from many orbits for many days, so the east-west asymmetry will not affect the results presented here. It should be noted that the essence of east-west asymmetry are commonly considered in analysis of SEP events at or inside geostationary orbit (e.g., Filwett et al., 2020; Rodriguez et al., 2010), where the difference between eastward and westward fluxes can be over one order magnitude because of the spatial gradient and the much larger gyroradius of SEP (at a weaker magnetic field).

We should also note that the results on Figure 3 are dominated by trapped populations, measured above SAA region (further illustrated in Figure 4), even though POES also measure drift/bounce loss cone particles, whose contributions are negligible.

2.3. Altitude Dependence and Comparison With AP9 Model

For highly inclined LEO spacecraft, the radiation dose is mainly due to inner belt protons, which increases with altitude because of the pitch angle distribution of the trapped protons. This altitude dependence is well recognized (e.g., Parsignault et al., 1981) and relates to mission design because of radiation effects on spacecraft (e.g., Miyake et al., 2014). The latest community-supported Aerospace Proton Model (AP9) has included this altitude dependence based on data from various missions, such as CRRES and Polar (Ginet et al., 2013. Also see https://www.vdl.afrl.af.mil/programs/ae9ap9/files/package/Ae9Ap9_v1_50_001_...
Here, we demonstrate the altitude dependence from SAMPEX/PET data of its first year’s measurements and compare them with AP9 model results.

A highly inclined LEO spacecraft can only measure trapped inner belt particles when it traverses the SAA region and measures SEP only at high latitudes. SAMPEX’s orbit had a procession period of ~110 days, with its apogee moving from the Southern Hemisphere to the Northern Hemisphere and back again.

The insert in Figure 4d shows the altitude of SAMPEX’s apogee and perigee early in the mission. Figures 4a and 4b show the location of SAMPEX/PET measurements of 27.4–37.4 MeV protons with flux greater than 0.01/(cm²-sr-MeV) around its apogee (673.4–692.5 km) and perigee (504.9–522.1 km), respectively, between 3 December 1992 and 21 September 1993. It is evident that most measurements of trapped protons were taken near the SAA, with much higher flux and more data points when apogee was in the Southern Hemisphere. It should be noted that measurements at high latitudes were during SEP events. The flux ratio between measurements taken around apogee and perigee is 1.85. This is almost a factor of two differences in radiation dose due to the proton flux between the altitude of 690 vs. 510 km for the same inclination. Figure 4 illustrates clearly that the radiation dose for a LEO spacecraft comes mostly from trapped inner belt protons around the SAA region, which is also important information for operating LEO spacecraft and instruments as they are all subject to such penetrating protons (e.g., Li et al., 2015), which have deleterious effects on various subsystems onboard and can affect intended measurements (e.g., Baker, 2002; Miyake et al., 2014).

Figures 4c and 4d show the 30-MeV proton flux (with a threshold of >0.01/(cm²-sr-MeV)) from the AP9 model calculated at SAMPEX’s location around its apogee and perigee. The local pitch angles of these measurements were taken to be between 30° and 80°, corresponding to the local pitch angle coverage of the SAMPEX/PET measurements. The flux ratio between apogee and perigee is 2.82, comparable to the actual SAMPEX/PET measurements.

It should be pointed out that the proton flux difference between the different altitudes is well reproduced by AP9 model. However, the solar cycle variation, which is much greater, with a flux ratio (maximum flux around solar min)/(minimum flux around solar max) of 4.5 around 500 km (as shown in Figure 2, top panel), is yet to be included in AP9 model (W. R. Johnston, private comm., 2019). The AP8 model has only two values for inner belt protons, corresponding to solar min and solar max. The same flux ratio of 30-MeV protons at $L = 1.4$ at 500 km is 1.6 (based on IRBEM-LIB, https://sourceforge.net/projects/irbem/), much smaller than what SAMPEX’s measurements show in Figure 4.

2.4. Van Allen Probes/REPT Measurements

Van Allen Probes, a pair of identical spacecraft, were launched into a geo-transfer-like orbit, with perigees of ~600-km altitude and apogees around 5.8 $R_E$ from the center of Earth and inclination of 10° on 30 August 2012 (Kessel et al., 2012; Mauk et al., 2012). The pulse-height-analyzed (PHA) data downloaded since October 2013 from the Relativistic Electron-Proton Telescope (REPT) (Baker, Kanekal et al., 2012; Spence et al., 2013) onboard the Van Allen Probes have been used to investigate the variation of 10s of MeV protons in the magnetosphere (Selesnick et al., 2014, 2016). The PHA data have also made it possible to extend the energy range of the original required measurements of REPT (24–76 MeV) to a much wider energy range: 18–600 MeV (Selesnick et al., 2018).

REPT, mounted on the side of the spacecraft that spins along the Sun-pointing axis, has a FOV of 32° and can measure particles with all equatorial pitch angles in the inner belt after a spin period (~11 s) (Baker, Kanekal et al., 2012). Figure 5a shows the 10-day averaged 27-MeV proton flux with equatorial pitch angles between 75–90° (black line) and 35–55° (blue line) at $L = 1.3$–1.4. The measured protons represented by the black line are stably trapped since the largest drift loss cone, in terms of equatorial pitch angle, at $L = 1.3$ is about 50° (which means a charged particle with an equatorial pitch angle just less than this would reach <100-km altitude in SAA and be lost into atmosphere). The protons represented by the blue line include both stably trapped protons (but closer to the drift loss cone) and quasi-trapped protons (with equatorial pitch angles less than 50°), which would be lost within a drift period. The pointing direction of the center of the FOV of REPT versus the local magnetic field can be accurately determined, but the angular resolution is still 16° from the pointing direction. The proton flux represented by the blue line, which is about one order of magnitude lower than the proton flux represented by the black line, not only includes protons with small equatorial pitch angles but also includes background from higher energy protons (Selesnick et al., 2018).
The background contribution to the blue line becomes significant but still negligible for the black line, as demonstrated in Figs. 3 and 4 in Selesnick et al. (2014).

It should be pointed out that the proton flux, in Figure 5a, with larger equatorial pitch angles (black line) is much greater than the proton flux with smaller equatorial pitch angles. Neither the black nor blue line shows any discernible solar cycle variation similar to that seen in the SAMPEX and POES data (Figures 2 and 3). This suggests that the sources and losses of inner belt protons mirroring close to the magnetic equator are different from those of inner belt protons measured at LEO. The latter have smaller equatorial pitch angles and a lower flux; they reach lower altitudes, thus subjecting them more to energy loss and pitch angle scattering from atmospheric collisions. In fact, trapped protons mirroring near the magnetic equator do show a solar cycle variation at lower L and a strong spatial gradient in their flux and variation at L < 1.2, as is discussed next.

2.5. Comparison Between Measurements and Model Results at Low L for Equatorially Mirroring Protons

Figure 6 shows the omnidirectional >36-MeV proton flux from June 2005 to February 2018 from POES-18 observations taken only near the magnetic equator with $B/B_{\text{min}} < 1.01$ (where $B_{\text{min}}$ is the magnetic field strength at the equator, based on the POES-18 orbit and the IGRF model), the corresponding simulation results based on a theoretical model (Selesnick & Albert, 2019), and REPT PHA data which are also converted to >36-MeV fluxes near the magnetic equator for direct comparison.

The simulation is based on the model described in Selesnick et al. (2007) with an extra loss equivalent to a mean lifetime of 22 years for the trapped protons (Selesnick & Albert, 2019), in addition to including energy loss due to collisions with free and bound electrons in the ambient plasma and neutral atmosphere, the direct loss due to inelastic nuclear scattering and detrapping during magnetic storms. The sources in the model are from CRAND and trapped energetic solar protons. The CRAND source rate is $S_n = \langle j_n \rangle / (v \tau)$, where $v$ is neutron speed, $\tau_{\text{n}}$ is the mean lifetime of a neutron, 887 s, and $\tau$ is the relativistic factor for a given neutron energy. The neutron intensity $j_n$ is drift averaged ($\langle j_n \rangle$), and itself is evaluated at the geographic location where the negative tangent to the trapped proton trajectory intersects the top of the atmosphere (100-km altitude). The energetic source neutron must be coming from the Earth (thus CRAND) and have the same direction of the proton, which attains the full kinetic energy and moves in the same direction as the decaying neutron. If there is no intersection for a given point on the trajectory then $j_n = 0$. The CRAND source for the inner radiation belt comes mostly from low geomagnetic latitude or high cutoff rigidity. The low-latitude neutron flux is relatively insensitive to solar cycle modulation because of the high cutoff rigidity (the GCR source corresponding to multiple GeV protons, which vary little over a solar cycle).
cycle). As for the SEP source, statistical studies of the injection efficiency as a function $L$, energy, and equatorial pitch angle are not yet available. Trajectory tracing simulations show how solar ion trapping and transport to low $L$ occurs (Hudson et al., 1997, 2004; Kress et al., 2005). The solar proton source rate is approximated as step function in $L$, $S_p > 0$ at $L \geq 2$ and $S_p = 0$ at $L < 2$. More detailed description is available in Selesnick et al. (2007). Radial diffusion is not included in the model here (for Figure 6) due to the very weak and uncertain radial diffusion rate at $L < 1.25$ (e.g., Schulz & Lanzerotti, 1974). The initial condition of this simulation was set 10 years ago. However, because we focus on 10s of MeV protons at lower $L$ regions, the loss process is rather dynamic (while the source is stable), the simulation results quickly lose memory of their initial values, reaching a dynamic balance of the current source and loss. The REPT PHA data were first processed to obtain the differential unidirectional proton flux as a function of the kinetic energy and the $L$ value of the proton guiding center and the equatorial pitch angle and were averaged over consecutive daily intervals (Selesnick et al., 2018; Selesnick & Albert, 2019). The differential unidirectional proton fluxes were integrated over equatorial pitch angles (following the eq. 5 of Selesnick et al. (2014)) to obtain omnidirectional proton fluxes and were integrated over kinetic energy to obtain the integral proton flux shown in Figure 6.

We note several outstanding features in Figure 6:

1. The REPT PHA flux compares well with POES flux when both of them are restricted to near the magnetic equator, which is remarkable considering the different instrument designs operating in different orbits.
2. The simulation results reproduce well the POES measurements for the main features: (i) no obvious solar cycle variation at \( L > 1.2 \) but clear solar cycle variation at \( L < 1.2 \) and the magnitude of the variation greatly enhance at lower \( L \), e.g., over one order of magnitude variation at \( L = 1.15 \) between solar max and min; (ii) a strong spatial gradient of the proton flux at \( L < 1.2 \), e.g., over one order of magnitude difference in flux between protons drifting at \( L = 1.15 \) and \( L = 1.17 \) near the magnetic equator (the spatial difference between these two drift shells is ~120 km); (iii) the spatial gradient itself is a strong function of \( L \), increasing significantly at lower \( L \) and decreasing at \( L > 1.2 \).

3. The phase lags between the proton flux (both simulation results and POES measurements) and the sunspot number are strikingly different at different \( L \). There is little phase lag at \( L = 1.15 \) (particularly in the simulation results), suggesting that proton energy loss is fast at low altitude (above the magnetic equator) and greatly enhanced during solar max (when the local atmospheric density enhanced). However, as \( L \) increases slightly, e.g., to \( L = 1.17 \) and \( L = 1.19 \) (equivalent to ~120-km distance between these two drift shells), the phase lag increases significantly. The phase lag between the simulation results and the sunspot number is estimated in a similar way in Figures 2 and 3, 37 days (229 days for POES), 165 days (357 days for POES), and 485 days (485 days for POES) for \( L = 1.15, 1.17, \) and 1.19, respectively.

For protons mirroring close to the magnetic equator, there is no obvious solar cycle variation at \( L > 1.2 \). This is very different from measurements taken at higher latitudes (as demonstrated in Figures 2 and 3, \( L = 1.33–1.42 \)) where the solar cycle variation is mainly due to enhanced loss of protons, which have smaller equatorial pitch angles and are already close to the drift loss cone, during solar max.

In the simulation model, there are several loss terms for the protons: energy loss due to collisions with free and bound electrons in the ambient plasma and neutral atmosphere, direct loss due to inelastic nuclear scattering, and detrapping during magnetic storms. In the low \( L \) region (<1.25), detrapping is negligible, and the inelastic nuclear scattering is not significantly compared to the energy loss due to collisions with free and bound electrons, which is the dominate loss mechanism and increases fast at lower \( L \). The source in this low \( L \) region is dominated by CRAND, as trapped energetic solar protons can hardly be radially diffused into such a low \( L \) region (Selesnick & Albert, 2019).

3. Summary and Conclusions

Motivated by the long-term measurements of GCR by V1 and V2, which show a clear solar cycle variation for ~300-MeV protons, we have investigated the solar cycle variations and local spatial variations of the trapped inner radiation belt protons. Based on the long-term measurements from SAMPEX, POES, and Van Allen Probes, we have demonstrated that the solar cycle variation of inner belt protons measured by LEO satellites is mainly due to enhanced loss during solar max since the variation of the corresponding cosmic rays (inferred from NM measurements at low latitude) is much smaller. We have also demonstrated that the inner belt proton intensity and solar cycle variation measured at LEO also depends sensitively on altitude. Such behavior of inner belt protons was predicted by theory decades ago (e.g., Blanchard & Hess, 1964) simply based on the source and loss mechanisms and also demonstrated with various satellites measurements (e.g., Huston & Pfitzer, 1998; Parsignault et al., 1981). Here, we have revisited this behavior and analyzed it in more quantitative detail, including comprehensive modeling of protons mirroring near the magnetic equator with direct comparison to measurements. Specific findings are as follows:

1. The flux ratio between measurements taken by SAMPEX around its apogee (690 km) and perigee (510) is 1.85, which is comparable to the AP9 model results (2.85) for the same altitudes. However, the flux ratio, (flux around solar min)/(flux around solar max), is 4.5 around 500 km from the solar cycle variation, which is not yet included in AP9 model. The same flux ratio of 30-MeV protons at \( L = 1.4 \) at 500 km from the solar cycle variation is only 1.6 based on AP8 model.

2. The relative solar cycle variation of the energetic proton flux at higher altitude (~860 km) becomes much smaller: only about 21.5% for >36-MeV protons and 21.4% for >140-MeV protons, suggesting that loss from the ionosphere and atmosphere becomes much less effective at higher altitudes.

3. The phase lags between the variation of the proton fluxes measured at LEO and the sunspot number increase significantly with the altitude of the measurement. The estimated phase lags are 154 days for SAMPEX measurements at ~500 km and 730 days for POES-18 measurements at ~860 km, again suggesting that loss from the ionosphere and atmosphere becomes much less effective at higher altitudes.
4. Another detailed feature of the sensitive dependence of the proton flux on altitude is demonstrated by POES-18 measurements. With a difference of only 21 km between POES-18’s apogee (869 km) and perigee (848 km), the relative variation of >36-MeV protons and >140-MeV protons near apogee and perigee in the Southern Hemisphere is 2.9% and 2.7%, respectively.

5. For the protons mirroring near the magnetic equator, both measurements and simulations show no obvious solar cycle variation at $L > 1.2$ but there are clear solar cycle variations at $L < 1.2$ and a strong spatial gradient of the proton fluxes and its variations as well at $L < 1.2$. The phase lag between the proton flux and sunspot number increases greatly from $L = 1.15$ to $L = 1.19$.

Based on the good comparison between the simulation and the measurements of protons mirroring near the magnetic equator, we conclude that the decay of the measured proton flux is mainly due to the energy loss of protons colliding with free and bound electrons in the ionosphere and atmosphere and this energy loss is strongly altitude dependent, as demonstrated in Figure 6. As discussed in (Selesnick & Albert, 2019), the specific mechanism responsible for the extra loss term equivalent to a mean lifetime of 22 years in the model is still elusive, which presents a challenging and unanswered question as to the actual physical mechanisms responsible for the loss of these trapped protons. Nonetheless, the finding of fast energy loss of the protons at low altitude due to collisions with free and bound electrons in the ionosphere and atmosphere holds, and these demonstrated characteristics are also important for future spacecraft and instrument design and operation in this space environment.

Data Availability Statement

The data for Voyager, Neutron Monitor, SAMPEX, and POES are all publicly available at https://cdaweb.gsfc.nasa.gov, respectively. Van Allen Probes REPT Level 1 data are available at www.rbsp-ect.lanl.gov. The sunspot number, F10.7 solar indices, and geomagnetic indices used in this study are obtained from the OMNI database (http://omniweb.gsfc.nasa.gov).

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