Dead reckoning localisation technique for mobile wireless sensor networks

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Abstract: Localisation in wireless sensor networks (WSNs) not only provides a node with its geographical location but also a basic requirement for other applications such as geographical routing. Although a rich literature is available for localisation in static WSN, not enough work is done for mobile WSNs, owing to the complexity because of node mobility. Most of the existing techniques for localisation in mobile WSNs use Monte Carlo localisation (MCL), which is not only time consuming but also memory intensive. They, consider either the unknown nodes or anchor nodes to be static. In this study, the authors propose a technique called dead reckoning localisation for mobile WSNs (DRLMSN). In the proposed technique all nodes (unknown nodes as well as anchor nodes) are mobile. Localisation in DRLMSN is done at discrete time intervals called checkpoints. Unknown nodes are localised for the first time using three anchor nodes. For their subsequent localisations, only two anchor nodes are used. The proposed technique estimates two possible locations of a node using Bézout’s theorem. A dead reckoning approach is used to select one of the two estimated locations. The authors have evaluated DRLMSN through simulation using Castalia simulator, and is compared with a similar technique called received signal strength-MCL proposed by Wang and Zhu (2008).

1 Introduction

Localisation is the process of providing each node with its geographical location. It is an important research issue in wireless sensor networks (WSNs). This is because each sensor node stamps the sensed data with its geographical location prior to transmission. The sink, distinguishes the received data based on the spatio-temporal characteristics, in which the location information is important and has a unique characteristic. Therefore the transmitting node must be aware of its geographical position.

Localisation not only provides the geographical position of a sensor node but also fills the pre-requisites for geographical routing, load balancing, spatial querying, data dissemination, rescue operations and target tracking [1–6]. Location-based routing can save significant amount of energy by eliminating the need for route discovery [7]. It can also improve the caching behaviour of applications where the requests are location dependent.

Mobility of sensor nodes increases the applicability of WSNs. The mobility of a sensor node with respect to environment can be of two types: (i) static and (ii) dynamic. In static, a sensor node is only data driven, that is, to sense the environment and report to the base station, whereas in dynamic a sensor node is not only data driven but also serves as an actuator. In both the cases, the position of nodes changes oftenly. As a result, a node in mobile WSNs is localised more than once, compared with static WSNs – where a node is localised only once at the initialisation of network. The continuous localisation of nodes with mobility results in (i) faster battery deletion and hence, reduces the lifetime of sensor nodes and (ii) increases the communication cost. In contrast, mobility improves (i) coverage of WSN – uncovered locations at one instant can be covered at some other instant of time, (ii) enhances the security – intruders can be detected easily as compared with the static WSNs, and (iii) increases connectivity – mobility increases the neighbours of a node [8].

The geographical position of a sensor node is determined either with the help of global positioning system (GPS) equipment or estimated from the location of neighbouring nodes. A network with all GPS enabled nodes is not a universal solution. This is because in addition to increasing the cost, size and power consumption; it fails to localise in indoors and dense forests. An alternative solution is to equip only a minimal number of nodes called ‘anchor nodes/seeds’ with GPS, and the remaining nodes estimate their location using the location information of anchor nodes. A mobile WSN can be in one of the following scenarios [7, 9–21]:

(1) Normal nodes are static and seeds are moving: In this scenario, mobile anchor nodes (≥1) continuously broadcast their location. As soon as a static node receives three or more beacons, it localises itself. Accuracy and localisation time depends mostly on the trajectory followed by the seeds.

(2) Normal nodes are moving and seeds are static: In this scenario, each normal node is expected to receive the beacons at the same instant of time. Otherwise, it results into inaccurate estimated location. With time span the
previous estimated location becomes obsolete. As a result, nodes localise repeatedly at fixed intervals with newly received seed locations. One of the appropriate example for this scenario is battlefield, where normal nodes are attached to military personnel and seeds are fixed a priori as landmarks within the battlefield. This not only helps in detecting the current position but also in providing feedback from a particular area of battlefield.

(3) Both the normal nodes and seeds are moving: This scenario is the most versatile, and complex among all the three. In this, the topology of the network changes very often. It is difficult for a normal node to obtain fine grained location. Therefore the localisation error is comparatively higher than the previous two scenarios.

In this paper, we propose a localisation technique for the scenario, where both the normal nodes and seeds are moving. We have considered this scenario because (i) a little emphasis is given, owing to its complexity and (ii) to the best of our knowledge whatever little localisation techniques exist for this scenario are range free based. The proposed technique is called dead reckoning localisation technique (DRLMSN). Owing to node mobility the position of nodes changes frequently. Localising the nodes at every instant will drain their battery power at a faster rate. Therefore in DRLMSN nodes are localised at discrete time intervals called checkpoints. Nodes are localised for the first time using the trilateration mechanism. In their subsequent localisations, only two anchor nodes are used. Bézout’s theorem [22] is used to estimate the positions of a node, and a dead reckoning technique is used to select the correct position. DRLMSN is compared with RSS-MCL [1].

The rest of the paper is organised as follows: Section 2 provides an overview of various localisation techniques. The proposed localisation algorithm is described in Section 3. Simulation and results are presented in Section 4 and conclusions are drawn in Section 5.

2 Related work

Localisation algorithms for WSNs can be broadly categorised into two types: ‘range based’, and ‘range free’. Range-based localisation algorithms uses range (distance or angle) information from the beacon node to estimate a sensor node’s location [23]. They need at least three beacon nodes to estimate the position of a node. Several ranging techniques exist to estimate the distance of a node to three or more beacon nodes. Based on this information, location of a node is determined. A few representative of range-based localisation algorithms include received signal strength indicator (RSSI) [24], angle-of-arrival(AoA) [25], time-of-arrival (ToA) [26], time difference of arrival (TDoA) [25]. These schemes often need extra hardware such as antennas and speakers, and their accuracy is affected by multi-path fading and shadowing.

Range-free localisation algorithms use only connectivity information between unknown node and landmarks – which obtain their location information using GPS or through an artificially deployed information. Some of the range-free localisation algorithms include centroid [27], appropriate point in triangle (APIT) [28] and DV-HOP [29]. Centroid counts the number of beacon signals it has received from the pre-positioned beacon nodes and achieves localisation by obtaining the centroid of received beacon generators. DV-HOP uses location of beacon nodes, beacon hop count and the average distance per hop for localisation. The APIT algorithm requires a relatively higher ratio of beacons to nodes and longer range beacons for localisation. They are susceptible to erroneous reading of RSSI. He et al. [30] showed that the APIT algorithm requires lesser computation than other beacon-based algorithms and performs well when the ratio of beacon to node is higher. A brief review of different localisation algorithms proposed in the literature for mobile sensor networks is presented below.

In [31], Tilak et al. proposed two classes of localisation approaches for mobile WSNs. They are (i) adaptive and (ii) predictive. Adaptive localisations dynamically adjust their localisation period based on the recent observed motion of the sensor, obtained from examining the previous locations. This approach allows the sensors to reduce their localisation frequency when the sensor is slow, or increase when it is fast. In the predictive approach, sensors estimate their motion pattern and project their future motion. If the prediction is accurate, which occurs when nodes are moving predictably, location estimation may be generated. However, their main focus was on how often the localisation should be done, and not on the localisation process itself.

Bergamo and Mazzimi [13] proposed a range-based algorithm for localising mobile WSNs. They used fixed beacons placed at two corners on the same side of a rectangular space. Mobile sensor uses beacon signals to compute their relative position. Sensors estimate their power level from the received beacon and compute their position by the triangulation method. They also studied the effect of mobility and fading on location accuracy. Placing beacons at fixed position limits the localisation area. This is because the quality of RSSI decreases with distance because of various factors. This results in inaccurate distance measurement.

Hu and Evans [7] proposed a range free technique based on Monte Carlo localisation (MCL). This technique is used for localisation of robots in a predefined map. It works in two steps: first, the possible locations of an unknown node are represented as a set of weighted samples. In the next stage, invalid samples are filtered out by incorporating the newly observed samples of seed nodes. Once enough samples are obtained, an unknown node estimates its position by taking the weighted average of the samples. In this technique, the sample generation is computationally intensive and iterative in nature. This also needs a higher seed density.

Aline et al. [32] proposed a scheme to reduce the sample space generated in [7]. They named it as Monte Carlo Boxed (MCB) scheme. Sample generation is restricted within the bounding box, which is built using 1-hop and 2-hop neighbouring anchor nodes. The neighbouring anchor information is also used in the filtering phase. The number of iterations to construct the sample space is reduced. However, the localisation error in MCB is not reduced, if the number of valid samples is the same as that in MCL.

Using the MCL technique, Rudafshani and Datta [33] proposed two algorithms called MSL and MSL*. Static sensor nodes are localised in MSL* too. It uses sample set of all 1-hop and 2-hop neighbour of normal nodes and anchor nodes. This resulted in better position estimation with increased memory requirement and communication cost. In MSL, a node weight its samples using the estimated position of common neighbour nodes. MSL* outperforms MSL in most scenarios, but incurs higher communication cost. MSL* outperforms MSL* when there is significant irregularity in the radio range. Accuracy of common
neighbouring nodes are determined by their closeness value. The closeness value of a node $P$ with $N$ samples is computed as

$$\text{Closeness}_P = \frac{\sum_{i=1}^{N} W_i \sqrt{(x_i - x)^2 + (y_i - y)^2}}{N}$$

where $(x, y)$ is $P$’s estimated position and $(x_i, y_i)$ is $P$’s $i$th sample with weight $W_i$. Both MSL and MSL* need higher anchor density and node density. Moreover, when maximum velocity is large, performance of both MSL and MSL* reduces to a greater extent. Furthermore, the size of bounding box for sample generation is reduced in [34], using the negative constraint of 2-hop neighbouring anchor nodes. This reduces the computational cost for obtaining samples, and a higher location accuracy is achieved under higher density of common nodes.

Wang and Zhu et al. [1] proposed the RSS-based MCL scheme which sequentially estimates the location of mobile nodes. First, it uses a set of samples with related weights to represent the posterior distribution of node’s location. Next, it estimate the node’s location recursively from the RSS measurement within a discrete state-space localisation system. Accuracy of this scheme depends on the number of samples used and the log normal statistical model of RSS measurements. It improves the localisation accuracy using both the RSSI and MCL techniques. However, it is time intensive to the sampling procedure. Moreover, the frequent sampling at regular intervals consume more energy of the nodes.

Comparison of different localisation techniques is shown in Table 1.

| Localisation technique | Type | Mechanism | Mobility model | Comments |
|------------------------|------|-----------|----------------|----------|
| Tilak et al. [31]      | range based | triangulation | random waypoint model (RWP), Gaussian Markovian model, RWP | emphasised on localisation frequency rather than localisation accuracy |
| Bergamo and Mazzini [13] | range based | triangulation | RWP, reference point group model [35] | limits the localisation area, consider static beacon nodes |
| Hu and Evans [7]       | range free | sequential MCL | modified RWP with pause time $\geq 0$ and minimum node speed $= 0.1$ m/s | slow in convergence, slower sampling technique, lesser the sample space, more the localisation error |
| Baggio and Langendoen [32] | range free | MCL boxed | modified RWP with pause time $= 0$ s | computationally intensive, higher communication cost, requires higher anchor and node density |
| Rudafshani and Datta [33] | range free | particle filtering | approach of MCL | accuracy depends on the sampling quality, and the RSSI model |
| Wang and Zhu [1]       | range based | sequential MCL | RWP | |

3 Dead reckoning localisation technique

In this section, we propose a range based, distributed localisation algorithm for mobile WSNs. The proposed technique is called the dead reckoning localisation technique (DRLMSN). Nodes in DRLMSN are classified into the following three types: (i) ‘anchor node (A)’: a node which can locate its own position, and is usually equipped with GPS, (ii) ‘normal/unknown node (U)’: nodes which are unaware of their location, and uses localisation algorithm to determine their position, and (iii) ‘settled node (S)’: these are normal nodes that have obtained their location information through a localisation technique. They serve as an anchor node for the remaining unknown nodes.

To localise normal mobile nodes accurately with the help of mobile anchor nodes is a difficult task. This is because the transmitter and the receiver change their position at every time instant. Therefore to localise, a normal node must receive ‘beacons’ from all the neighbouring nodes at the same time instant. ‘Beacons’ are frequently advertised from the anchor/settled nodes. This advertisement contains the anchor/settled ‘node’s identity’ and ‘location’. Continuous localisation of mobile nodes will drains their battery power at a faster rate. As a result, the lifetime of sensor nodes as well as the sensor network is reduced.

Sensor nodes in DRLMSN are localised during a time interval called ‘checkpoint’. There are two localisation phases in DRLMSN. First phase is called ‘initialisation’ phase. In this phase, a node is localised using the trilateration mechanism. A node remains in the initialisation phase until it localises using the trilateration mechanism. The subsequent localisation phase is called ‘sequent’ phase. In this phase, a node localises itself using only two anchor nodes. Bézout’s theorem [22] is used to estimate locations of a node. A ‘dead reckoning’ approach is used to identify their correct estimated position. Once a node is localised in either of the above two phases, it act as a settled node and broadcast beacons during the checkpoint. Initialisation and sequent phases are explained below.

### 3.1 Initialisation phase

At the beginning of a ‘checkpoint’, each anchor node broadcasts a beacon. A normal node localises itself for the first time during the checkpoint using three anchor nodes. As soon as, a node localises, it broadcasts a beacon during the same checkpoint. This results in the localisation of one/two beacon deficit nodes. This process continues until the end of the checkpoint.

At the end of the checkpoint, some nodes may fail to localise. The possible reasons for localisation failure and the corresponding actions to be taken are (i) ‘A normal node receives only one (or two) beacon’. In this case, normal node deletes the received beacons and moves on. In the subsequent checkpoint it attempts to localise using three beacons. (ii) ‘A normal node receives no beacon’. In this case, a node moves on and attempts to localise itself in the next checkpoint using three beacons.

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**Table 1** Comparison of different localisation techniques for mobile WSN

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3.2 Sequent phase

A node goes to the sequent phase only after itself localises using the trilateration mechanism. In this phase, each normal node localises with only two nearest location aware nodes (‘anchor/settled node’). A normal node that receives two beacons can estimate its two positions using Bézout’s theorem. According to Bézout’s theorem ‘The intersection of a variety of degree m with a variety of degree n in complex projective space is either a common component or it has mn points when the intersection points are counted with the appropriate multiplicity’. Positions estimation of a node using Bézout’s theorem is explained below.

Let \( (x, y) \) be the position of an unknown node and \( (a_1, b_1), (a_2, b_2) \) be the position of two of its neighbouring anchor nodes. Moreover, let the distance between an unknown node and the respective anchor nodes be \( d_1 \) and \( d_2 \), respectively. Then

\[
(x - a_1)^2 + (y - b_1)^2 = d_1^2 \\
(x - a_2)^2 + (y - b_2)^2 = d_2^2
\]

Re-arranging (1) and (2), we obtain

\[
x^2 + y^2 = a_1^2 - a_1^2 - b_1^2 + 2a_1x + 2b_1y \\
x^2 + y^2 = a_2^2 - a_2^2 - b_2^2 + 2a_2x + 2b_2y
\]

Comparing (3) and (4), we have

\[
d_1^2 - a_1^2 - b_1^2 + 2a_1x + 2b_1y = d_2^2 - a_2^2 - b_2^2 + 2a_2x + 2b_2y \\
2(a_1 - a_2)x = (a_1^2 - a_1^2 - b_1^2 - d_1^2 + a_1^2 + b_1^2) \\
+ 2(b_2 - b_1)y
\]

Let \( z_0 = d_2^2 - a_2^2 - b_2^2 - d_1^2 + a_1^2 + b_1^2 \).

The (6) can be reduced to

\[
x = \frac{z_0 + 2(b_2 - b_1)y}{2(a_1 - a_2)} \tag{7}
\]

For simplification, this can be written as

\[
x = z + py \tag{8}
\]

where \( z = (z_0/2(a_1 - a_2)) \) and \( p = (2(b_2 - b_1)/2(a_1 - a_2)) \).

Substituting the value of \( x \) in (1), we obtained

\[
(p^2 + 1)y^2 + (2p - 2a_1p - 2b_1)y \\
y - (d_1^2 - a_1^2 - b_1^2 - z^2 + 2a_1z) = 0 \tag{9}
\]

Solving the quadratic (9), let the values obtained be \( y_1 \) and \( y_2 \). Let \( x_1 \) and \( x_2 \) be the values corresponding to \( y_1 \) and \( y_2 \), respectively. Therefore the proposed algorithm estimates two positions \( P_1(x_1, y_1) \) and \( P_2(x_2, y_2) \).

In order to select the correct estimated position a ‘dead reckoning’ approach is used. In this approach, a localised node say \( k \) uses the location, \( p_{v_{\text{prev}}} \) at the checkpoint \( t_i \) to estimate its location in the next checkpoint at \( t_{i+1} \). Let \( v \) be the velocity and \( t \) be the time interval between the two successive checkpoints. Distance \( d \) travelled by the node \( k \) between two successive checkpoints is calculated as \( d = v^t \).

Therefore at the checkpoint \( t_{i+1} \), an unknown node knows its position at checkpoint \( t_i \) and the distance \( d \) travelled between the two successive checkpoints. Moreover, the node has two anchor positions, that is, \( (a_1, b_1), (a_2, b_2) \).

Then, the node uses trilateration to calculate the position \( P(\tilde{x}, \tilde{y}) \). Next, the node computes the correction factor (CF) to select one of the two estimated positions \( P_1 \) and \( P_2 \). The correctness factor is computed as

\[
\text{Cf}_1 = \sqrt{(\tilde{x} - x_1)^2 + (\tilde{y} - y_1)^2} \\
\text{Cf}_2 = \sqrt{(\tilde{x} - x_2)^2 + (\tilde{y} - y_2)^2}
\]

**Fig. 1** Initialisation phase

\( a \) At the first checkpoint, anchor nodes transmit beacons, and normal nodes become localised via trilateration

\( b \) Normal nodes that are short of 1 or 2 beacons becomes localised with the help of settled nodes
where \(C_{f_1}\) and \(C_{f_2}\) represent the distance of position \(P_1\) and \(P_2\) from the position \(P\) estimated via trilateration. The correct position of the node is \(P_1(x_1, y_1)\) if \(C_{f_1} < C_{f_2}\) else the correct position is \(P_2(x_2, y_2)\). This is because, calculated position \(P(\hat{x}, \hat{y})\) always deviate from the actual position by a small margin. Once a node is localised, it broadcasts beacons until the end of the checkpoint.

We illustrate the localisation process in the proposed scheme using Fig. 1. Localisation in the initialisation phase is shown in Figs. 1a and b. Node 3 in Fig. 1a receives beacon from three anchor nodes 0, 1 and 2 at checkpoint \(t_i\) and becomes localised. Nodes 4 and 7 receive only two beacons, whereas nodes 5, 6 and 8 receives only one beacon. These nodes at this point of checkpoint \(t_i\) cannot localise, as the number of beacons required for localisation for the first time is three. Node 3 broadcast a beacon after localisation. Nodes 4 and 7 become localised after receiving beacon from node 3. This is shown in Fig. 1b. This co-operative, the distributive process of localisation continues until the end of the checkpoint. At the end of the checkpoint \(t_i\), nodes 6 and 8 have only one beacon. Both the nodes delete the received beacons and continues moving.

Fig. 2b illustrates the sequent phase at checkpoint \(t_{i+1}\). We consider node 3, to explain localisation using two anchor nodes. Let the co-ordinate of node 3 at checkpoint \(t_i\) be \((5.5, 6.3)\) as shown in Fig. 2a, and the distance traversed during the checkpoint interval \(t_i\) and \(t_{i+1}\) be 3.5 unit. At checkpoint \(t_{i+1}\), node 3 can be localised using two anchor nodes 0 and 2, as shown in Fig. 2b. Let the co-ordinates of node 0 and 2 be \((7, 8)\) and \((11, 6)\), respectively, as shown in Fig. 2b. Using Bézout’s theorem node three estimates two locations \(P_1(8.54, 5.54)\) and \(P_2(9.98, 8.24)\). To select one of the above two locations dead reckoning approach is used. Based on the location of node 0, node 2 and its previous location, node 3 estimates its new location \(P(\hat{x}, \hat{y})\) is equal to \((8.78, 6.03)\) using the trilateration technique. Then, node 3 calculates the correctness factor \(C_{f_1}\) and \(C_{f_2}\) to find the least deviated estimated position from \(P(\hat{x}, \hat{y})\). The computed value of \(C_{f_1}\) and \(C_{f_2}\) is 0.738 and 2.514, respectively. Since \(C_{f_1} < C_{f_2}\), the position \(P_1(8.54, 5.54)\) is selected as the correct estimated position. It can be observed from Fig. 2b the actual position of node 3 is very close to the estimated position.

The proposed localisation algorithm is given as Algorithm 1 (see Fig. 3).

**Description of Algorithm 1:** The above algorithm is called at each node in the start of each checkpoint. In each checkpoint, anchor nodes broadcast beacons. This is mentioned in lines 5–7 of Algorithm 1 (Fig. 3). Lines 12–17 localise a node in the initialisation phase. In this phase a node needs three beacons and becomes localised via trilateration. Sequent phase localisation is mentioned in lines 18–22. In this phase a node require only two beacon nodes for localisation. This phase uses dead reckoning approach for the unambiguous localisation of unknown node. Lines 6, 14 and 20 in the algorithm do the job of beacon broadcast.

### 4 Performance evaluation

We have simulated the proposed scheme using Castalia simulator [36] that runs on the top of OMNET++. We have made the following assumptions in our simulation: (i) nodes are considered to be homogeneous, with respect to transceiver power and receiver sensitivity. This helps in controlling the connectivity between nodes in the network easily; (ii) for simplicity, we consider the transmission range of all the nodes as a perfect circle; and (iii) all the three beacon nodes are synchronised. This results in the accurate localisation of unknown nodes which otherwise tries to localise with obsolete beacons.

The key metrics used for evaluating the localisation algorithm is the accuracy in location estimation. We have calculated the estimated error as the difference between the estimated position and the actual position. The average root mean square error (RMSE) is calculated as

\[
\text{Average RMSE} = \frac{\sum_{i=1}^{N-P} ||\theta_i - \hat{\theta}_i||}{N - P}
\]

where \(\hat{\theta}_i\) is the estimated position, \(\theta_i\) is the actual position, \(N\) is the total number of nodes in the network and \(P\) is the number of anchor nodes.

We have considered the following parameters in our simulation: (i) nodes are randomly deployed in a sensor field of area \(200 \times 200\) m\(^2\); (ii) symmetric communication...
Algorithm 1

Notations: \(A\): Anchor node, \(U\): Unknown node, \(S\): Settled node

Variables for \(U\) and \(S\):

1. beaconSet \(\leftarrow \emptyset\) /* Set of received locations \((x,y)\).* /
2. locfirst \(\leftarrow 0\) /* Set to 1, if \(U\) has completed initialisation phase. */
3. \(P_{\text{prev}} \leftarrow -1\) /* Stores current estimated position of \(S\) used in next checkpoint. */
4. Status /* Indicates node type: its value can be \(A\) or \(U\) or \(S\). */

/* This algorithm is distributed and event oriented in nature. So, in each node type \((A, U, S)\) different actions get fired according to event triggered (recursive time interval for checkpoint or beacon reception). */

For Anchor Node:
5. if Status = \(A\) then
6. broadcast beacon
7. exit

For Unknown/Settled Node:
8. if Status \(= U\) then
9. repeat steps 10 and 11 until
   
10. \(R \equiv (\text{sizeof(beaconSet)} \geq 3) \text{ AND } (\text{locfirst} = 0) \text{ OR } \big((\text{sizeof(beaconSet)} \geq 2) \text{ AND } (\text{locfirst} = 1)\big)\) AND (End of Checkpoint)
11. received beacon /* A node monitors the beacon until the end of checkpoint or either one of the following happens: 1. Unknown node has received three beacons. 2. Settled node has received two beacons. */
12. beaconSet \(\leftarrow\) beaconSet \(\cup\) {beacon}
13. if (sizeof(beaconSet) \(\geq 3\) and (locfirst = 0)) then /* Initialisation phase. */
14. Position \(\leftarrow\) Trilateration(beaconSet)
15. broadcast beacon /* Localise using Trilateration. */
16. \(P_{\text{prev}} \leftarrow \) Position
17. locfirst \(\leftarrow 1\)
18. Status \(\leftarrow S\)
19. else if (sizeof(beaconSet) \(\geq 2\) and (locfirst = 1)) then /* Sequant phase. */
20. Position \(\leftarrow\) Use beaconSet and \(P_{\text{prev}}\)
21. broadcast beacon /* Localise using dead reckoning. */
22. \(P_{\text{prev}} \leftarrow \) Position
23. Status \(\leftarrow S\)
24. else /* \(A\) or \(S\) do not need beacon as these are localized already */
25. delete beacon
26. while ((End of checkpoint) AND (Status = \(S\) OR \(U\))) do
27. beaconSet \(\leftarrow\) \(\emptyset\) /* At the end of checkpoint delete received beacons. */
28. Status \(\leftarrow U\) /* For localising in next checkpoint settled node changes status to \(U\). */

/* Within different checkpoints a node remember only the values of \(P_{\text{prev}}\) and locfirst. */

Fig. 3 DRLMSN localisation algorithm

within a communication range of 20 m; (iii) anchor node density is 10%. We have defined the anchor density as the ratio between the anchor nodes to the total nodes in the network; (iv) transmission power is \(-5\) dBm; (v) path loss exponent (\(\eta\)) is 2.4; and (vi) the modified random waypoint mobility model (RWMM) [37] and the random direction mobility model (RDMM) [38]. We have compared DBNLE with another range-based localisation technique called RSS-MCL proposed by Wang and Zhu [1]. Through simulation, we studied the impact of the mobility model, anchor density, node speed, number of normal nodes and deployment topology on location estimation. Each of the above parameter is explained below.

Impact of mobility model: Mobility pattern plays an important role in the localisation process. In addition to increasing the network connectivity and coverage area, mobility affects the localisation accuracy, also drains the battery quickly, and the percentage of localised nodes. We considered two mobility models (i) the RWMM, (ii) RDMM and have shown the effect of mobility model on localisation accuracy.

In the RWMM, a node randomly chooses a new destination in a direction between \([0, 2\pi]\) and moves towards that destination with a speed in the range \([v_{\text{min}}, v_{\text{max}}]\). While in RDMM, a node randomly chooses a direction between \([0, 2\pi]\), a speed in the range \([v_{\text{min}}, v_{\text{max}}]\) and moves in the
chosen direction up to the boundary of the network. After reaching the boundary the same process is repeated. In both RWMM and RDMM, a node pauses for some predefined time before changing its direction. We have set the pause time to be zero, in order to simulate a continuous mobility model. From Fig. 4 it is observed that the RWMM have lower average RMSE than RDMM, as shown in Fig. 5. The reason for this difference in error is because of mobility pattern of nodes. In the RWMM, nodes mostly move within the vicinity of the centre. They are less likely to move towards the boundaries of the network, as shown in Fig. 6. Therefore a node will have relatively higher number of neighbours. As a result, a normal node selects the most nearest neighbours which results in lesser inaccuracy. In contrast to this, a node moves uniformly throughout the field in RDMM, as shown in Fig. 7. This type of movement does not favour the selection of best neighbours, because a node is surrounded by lesser number of neighbours. It is observed from Figs. 4 and 5 that average RMSE is lesser in DBNLE compared with RSS-MCL. This is because in RSS-MCL the number of beacons used to filter the generated sample is more compared with DBNLE which uses only 2–3 beacons. Owing to mobility, increasing dependence on the number of beacons used increases the uncertainty in position estimation. Among the two mobility models, RDMM increases network coverage whereas RWMM increases the connectivity among nodes.

**Impact of anchor nodes:** For a fixed network size, increasing the anchor density results in the localisation of more nodes in lesser time. This is because most of the nodes obtain higher number of anchor nodes as their neighbour. To find the effect of anchor density on localisation error we varied the anchor density between 5 and 20% keeping the total number of nodes to be fixed at 200. The plot for anchor density against localisation error in the RWMM and RDMM is shown in Figs. 8 and 9, respectively. It is observed from the figures that the average RMSE decreases with the increase in the anchor density. This is because: (i) higher the anchor density, lesser the number of nodes to be localised; (ii) a node gets more number of accurate beacons – resulting in lesser error accumulation and propagation. It is also observed that with an increase in anchor density the average rate of decrease of RMSE is higher, and at a higher anchor density the rate of decrease is lesser. Increase in the number of anchors does not affect average RMSE to a greater extent in RSS-MCL as compared with DBNLE. This is because in the RSS-MCL position estimation depends heavily on the quality of sample generation where as in DBNLE it directly depends on the number of beacons received. Furthermore,
average RMSE is lesser in the RWMM as compared with the RWDM. This is attributed to the neighbour density. In the RWMM, a node has higher neighbour density as compared with the RDMM.

Impact of node speed: The effect of speed on average RMSE by varying the anchor and node density is shown in Figs. 4, 5, 8 and 9. It is observed from the above figures that with increase in speed the localisation error also increases. Above figures show that the location estimation of a node in mobile WSNs is greatly affected by the node speed. A node covers more distance per unit time at higher speed. This increase in speed results in: (i) increase in the uncertainty of localising a node accurately, as the area over which a node needs to be localised increases, (ii) with the increase in distance covered, multi-path fading and shadowing comes into play. This affects the distance measurements and decreases the efficiency of range-based localisation algorithm, (iii) it also affects the basic functionality, that is, sensing is not properly done when a node moves too fast, (iv) it increases the localisation percentage in low anchor density networks because increase in speed increases the network coverage.

Impact of normal nodes: The plot for normal nodes against localisation error is shown in Figs. 4 and 5, respectively. With increase in the number of normal nodes there is a significant increase in the percentage of localised nodes. This also results in the decrease of localisation time and localisation error. Decrease in localisation time is attributed to more number of localised neighbours of a normal node. It is observed from Figs. 4 and 5 that localisation error decreases gradually with the increase of nodes. The reason for this decrease is the selection of more number of nearest in-range neighbours. Closer is the neighbour lesser is the ranging error; as the quality of signal (RSSI) is directly affected by the distance between the transmitter and receiver node.

Impact of deployment/topology of nodes: Next, we consider the effect of deployment on localisation error. We have considered two deployment scenarios: (i) random and (ii) grid to study their effect on localisation error. It is observed that in some cases nodes do not localise early and takes longer time to localise. Consequently, this increases the localisation time of whole network. This is because of the non-availability of requisite number of beacons for localisation. One of the major reasons for this is the way in which nodes are deployed initially and the manner in which nodes move. It is observed that if nodes are randomly deployed, then 30% of the nodes fail to localise in the first
2–3 checkpoints, whereas in grid network around 90% of nodes localise in the first checkpoint itself. In the next checkpoint all nodes become localised. From Figs. 10 and 11, it is observed that the localisation error is lesser in grid deployment than in random deployment.

Finally, we studied the percentage of nodes localised at different checkpoints. The plot for percentage of localised nodes against checkpoints is shown in Figs. 12 and 13. It is observed that the percentage of nodes localised increases as the checkpoint increases. Majority of the nodes becomes localised after the fourth checkpoint. Percentage of localised nodes in RSS-MCL is relatively lesser as compared in DRLMSN. This is because the time spent in sample generation and filtering is more than checkpoint duration. As a result, most of the nodes fail to localise in RSS-MCL because of this time constraint.

### 5 Conclusions

A large number of localisation techniques have been developed for static WSNs. These techniques cannot be applied to mobile WSNs. Only a few localisation techniques have been proposed for mobile WSNs. Most of these techniques considered either normal node or anchor nodes to be static. In this paper, we propose a technique called dead reckoning localisation for mobile WSN. We have considered both the normal nodes and anchor nodes to be mobile. As the nodes move in a sensor field, their position changes with time. Therefore a mobile node has to be localised as long as it is alive. In the proposed technique, nodes are localised at discrete time intervals called checkpoints. A normal node is localised for the first time using three anchor nodes. For their subsequent localisations only two anchor nodes are used and a dead reckoning technique is applied. Reduction in the number of anchor nodes required for localisation from three to two results in faster localisation and lesser localisation error. We have compared the proposed scheme with an existing similar scheme called RSS-MCL. It is observed that the proposed scheme has faster localisation time with lesser localisation error than RSS-MCL. We have also studied the impact of node density, anchor density, node speed, deployment type and mobility pattern on localisation. It was observed that the above parameters have strong influence in the localisation time and localisation error.

In future we would like to check the validity of DRLMSN with different mobility models other than RWMM and RDMM. Also, to implement the proposed scheme in a real environment and check its performance.

### 6 References

1. Wang, W.D., Zhu, Q.X.: ‘RSS-based Monte Carlo localisation for mobile sensor networks’, *IET Commun.*, 2008, 2, (5), pp. 673–681
2. Caruso, A., Chessa, S., De, S., Urpi, R.: ‘GPS free coordinate assignment and routing in wireless sensor networks’. IEEE INFOCOM, 2005, pp. 150–160
3. Dopico, N.J., Haro, B.B., Macua, S.V., Belanovic, P., Zazo, S.: ‘Improved animal tracking algorithms using distributed Kalman-based filters’. European Wireless, 2011, pp. 631–638.
4. Patwari, N., Ash, J.N., Kyperountas, S., Hero III, A.O., Moses, R.L., Correal, N.S.: ‘Locating the nodes: cooperative localization in wireless sensor networks’. *IEEE Commun. Mag.*, 2005, 43, (4), pp. 54–64
5. Yu, R., Zhang, Y., Yang, K., Xie, S., Chen, H.-H.: ‘Distributed geographical packet forwarding in wireless sensor and actuator networks – a stochastic optimal control approach’. *IET Wirel. Sensor Syst.*, 2012, 2, (1), pp. 63–74
6. Rightower, J., Borrelli, G.: ‘Localization systems for ubiquitous computing’. *Computer*, 2001, 34, (8), pp. 57–66
7. Hu, L., Evans, D.: ‘Localization for mobile sensor networks’. Proc. 10th annual Int. Conf. Mobile Computing and Networking, Mobihoc ’04, Philadelphia, PA, USA, 2004, pp. 45–57
8. Liu, Y., Yang, Z.: ‘Localization for mobile networks’, in ‘Location, localization, and localizability’, (Springer, 2011, 1st edn.), pp. 97–109
9. Galstyan, A., Krishnamachari, B., Lerman, K., Patttem, S.: ‘Distributed online localization in sensor networks using a moving target’. Third Int. Symp. Information Processing in Sensor Networks (IPSN), ISBN 04, 26–27 April 2004, pp. 61–70
10. Pathirana, P.N., Bulusu, N., Savkin, A.V., Jha, S.: ‘Node localization using mobile robots in delay-tolerant sensor networks’. *IEEE Trans. Mob. Comput.*, 2005, 4, (3), pp. 285–296
11. Suo, K.-F., Ou, C.-H., Jiao, H.C.: ‘Localization with mobile anchor points in wireless sensor networks’. *IEEE Trans. Veh. Technol.*, 2005, 54, (3), pp. 1187–1197
12. Jiang, J., Han, G., Xu, H., Shu, L., Guizani, M.: ‘LMAT: localization with a mobile anchor node based on trilateration in wireless sensor networks’. Global Telecommunications Conf. (GLOBECOM 2011), 2011 IEEE, 5–9 December 2011, pp. 1–6
13. Bergamo, P., Mazzimi, G.: ‘Localization in sensor networks with fading and mobility’. 13th IEEE Int. Symp. Personal, Indoor and Mobile Radio Communications, 15–18 September 2002, vol. 2, pp. 750–754
14. de Oliveira, L.L., Martins, J.B., Dessbesell, G., Monteiro, J.: ‘CentroidM: a centroid-based localization algorithm for mobile sensor networks’. Proc. 23rd Symp. Integrated Circuits and System Design, SBCCI ’10, New York, NY, USA, 2010, pp. 204–209
15. Sheu, J.-P., Wu, W.-K., Lin, J.-C.: ‘Distributed localization scheme for mobile sensor networks’. *IEEE Trans. Mob. Comput.*, 2010, 9, (4), pp. 516–526
16. Wang, Z., Wang, Y., Ma, M., Wu, J.: ‘Efficient localization for mobile sensor networks based on constraint rules optimized Monte Carlo method’, *Comput. Netw.*, 2013, 57, (14), pp. 2788–2801
17. Rad, H.J., Aman, A., Leis, G.: ‘Cooperative mobile network localization via subspace tracking’. IEEE Int. Conf. Acoustics, Speech and Signal Processing, ICASSP ’11, 2011, pp. 2612–2615
18. Savic, V., Zazo, S.: ‘Cooperative localization in mobile networks using nonparametric variants of belief propagation’, *Ad Hoc Netw.*, 2013, 11, (1), pp. 138–150
19. Nicolli, M., Gezici, S., Sahinoglu, Z., Wymeersch, H.: ‘Localisation in mobile wireless and sensor networks’, *EURASIP J. Wirel. Commun. Netw.*, 2011, 2011, (1), pp. 1–3
20. Rashid, H.: ‘Localization in wireless sensor networks’, Master’s thesis, National Institute of Technology Rourkela, India, 2013
21. Chen, H., Gao, F., Martins, M., Huang, P., Liang, J.: ‘Accurate and efficient node localization for mobile sensor networks’, *Mob. Netw. Appl.*, 2013, 18, (1), pp. 141–147
22. Watkins, T.: ‘Bezout’s Theorem’. Available from http://www.sjsu.edu/~faculty/watkins/bezout.htm
23. Akyildiz, I.F., Vuran, M.C.: ‘Localization’, in ‘Wireless sensor networks’, (John Wiley and Sons Ltd, 2010), pp. 265–284
24. Zheng, J., Wua, C., Chua, H., Xua, Y.: ‘An improved RSSI measurement in wireless sensor networks’, *Procedia Eng. (Elsevier)*, 2011, 15, pp. 876–886
25. Boukerche, A., Oliveira, H.A.B.F., Nakamura, E.F., Loureiro, A.A.F.: ‘Localization systems for wireless sensor networks’. *IEEE Wirel. Commun.*, 2007, 14, (6), pp. 6–12
26 Ward, A., Jones, A., Hopper, A.: ‘A new location technique for the active office’, IEEE Personal Commun., 1997, 4, (5), pp. 42–47
27 Bulusu, N., Heidemann, J., Estrin, D.: ‘Gps-less low-cost outdoor localization for very small devices’, IEEE Personal Commun., 2000, 7, (5), pp. 28–34
28 Li, X., Shi, H., Shang, Y.: ‘A partial-range-aware localization algorithm for ad-hoc wireless sensor networks’. Proc. 29th Annual IEEE Int. Conf. Local Computer Networks, LCN ’04, 16–18 November 2004, pp. 77–83
29 Wang, Y., Wang, X., Wang, D., Agrawal, D.P.: ‘Range-free localization using expected hop progress in wireless sensor networks’, IEEE Trans. Parallel Distrib. Syst., 2009, 20, (10), pp. 1540–1552
30 He, T., Huang, C., Blum, B., Stankovic, J., Abdelzaher, T.: ‘Range free localization schemes in large scale sensor networks’. Proc. Ninth Annual Int. Conf. Mobile Computing and Networking, MobiCom ’03, 14–19 September 2003, pp. 81–95
31 Tilak, S., Kolar, V., Abu-Ghazaleh, N.B., Kang, K.D.: ‘Dynamic localization control for mobile sensor networks’. 24th IEEE Int. Conf. Performance, Computing, and Communications, IPCC ’05, 7–9 April 2005, pp. 587–592
32 Baggio, A., Langendoen, K.: ‘Monte Carlo localization for mobile wireless sensor networks’, Ad Hoc Netw., 2008, 6, (5), pp. 718–733
33 Rudareshani, M., Datta, S.: ‘Localization in wireless sensor networks’. Proc. Sixth Int. Conf. Information Processing in Sensor Networks, ISPN ’07, Cambridge, MA, USA, 2007, pp. 51–60
34 Slageng, Z., Cao, J., Lijun, C., Daoxu, C.: ‘Locating nodes in mobile sensor networks more accurately and faster’. Fifth Annual IEEE Communications Society Conf. Sensor, Mesh and Ad Hoc Communications and Networks, SECON ’08, 16–20 June 2008, pp. 37–45
35 Roy, R.R.: ‘Reference point group mobility’, in ‘Handbook of mobile ad hoc networks for mobility models’ (Springer, 2011), pp. 637–670
36 Boult, A.: ‘Castalia: a simulator for wireless sensor networks and body area networks’ (NICTA: National ICT Australia, 2011)
37 Schindelhauer, C.: ‘Mobility in wireless networks’. Proc. 32nd Annual Conf. Current Trends in Theory and Practice of Computer Science, SOFSEM ’06, Berlin, Heidelberg, 2006, pp. 100–116
38 Royer, E.M., Michael Melliar-Smithy, P., Moser, L.E.: ‘An analysis of the optimum node density for ad hoc mobile networks’. IEEE Int. Conf. Communications, ICC, 2001, vol. 3, pp. 857–861