Correlation of lithofacies and depositional environment using Markov chain analysis in Sambipitu formation at Ngalang river, Gunungkidul, Yogyakarta, Indonesia

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Abstract. The research area is located at Ngalang river, Gedangsari sub-district, Gunungkidul Regency, Special Region of Yogyakarta. The research area is part of southern mountain area which is composed of lithology of Sambipitu calcareous sandstone. The depositional process phase in the Sambipitu formation has a unique pattern and is relevant to the previous lithology. As a result, the stratigraphic position and lithological repetition pattern were reviewed using the statistical method (Markov chain). The aim of this research is to use geostatistics to examine the sedimentation trend in order to predict the existence of rock facies in the Sambipitu formation. In each unit of lithology cycle, geostatistics is expected to assist, predict and interpret the significance of subsequent lithology appearances. The research method used was measured stratigraphy, determination of rock age and depositional environment based on fossil identification. In addition, this research used probability matrix in Markov chain analysis. The results of the Markov chain analysis showed that lithology of rock in the upper Sambipitu formation had a non-random transition pattern. The results of statistical calculation showed that the calculation value was greater than the Chi-square table value (333.9>34.38) therefore the H₀ component was rejected. Lithofacies and depositional environment are correlated to several geological aspects such as distribution of rock facies, source of rock, paleobathymetri, trace fossils and sedimentation process.

Keywords: Stratigraphy; Markov chain; Correlation; Facies; Sambipitu

1. Introduction

Geological conditions define tectonic activities, basin settings, and sequence of rocks or stratigraphic (Suprapto et al., 2017). The implementation of statistics in geological science has not been recognized able to solve any problem related to geological condition, especially for pattern of lithology and facies cycle. In order to characterize surface and subsurface variability and related instability, geostatistical approaches have been used extensively (Michael et al., 2010). For example, a study by Jun et al. (2019) used special seismic oceanography to estimate speed and temperature using seismic data. The geostatistics was also applied to determine the depositional environment. Furthermore, the significance of vertical facies in Australia could be determined
with Markov chain analysis as well (He et al., 2019). Another study by Apriani (2016) used Markov chain analysis to estimate the developed lithology and depositional environment in West Sumatra.

The Sambipitu formation is part of southern mountain zone (van Bemmelen, 1949), which has been studied by numerous researchers. The presence of Sambipitu formation has an important aspect for stratigraphy analysis due to the stratigraphic position of Sambipitu, which is located between the volcanism period and post volcanism period (Surono et al., 1992). Bothe (1929) and Pandita (2008) reviewed about geological aspect specifically in stratigraphy. The research area of this study is located in the southern mountain zone, specifically at the Ngalang River, Gedangsari Sub-district, Gunungkidul Regency, Indonesia. The geological data were collected by observing the outcrop along the Ngalang river. The upper part of rock distribution in the Ngalang river is dominated by calcareous rock composition with several trace fossils (Rizqi & Purnomo, 2019). Pramunita & Pandita (2020) reported that the trace fossils consisted of several ichnofacies that were successfully identified as scoyenia, skolithos, cruziana, and zoophycos. There have been several geological qualitative studies conducted in the Ngalang River. However, the geostatistics researches that are related to depositional environment specifically in quantitative analysis (Markov chain) have never been done before.

This research used a quantitative descriptive method with Markov chain analysis. Markov chain analysis combines the geological data (qualitative data) and statistics data (quantitative data). The purpose of this research is to identify lithofacies and facies model and also to determine the correlation of Markov analysis and depositional environment. The rock lithology of the Sambipitu formation is made up of clastic and carbonate rocks. The Markov chain method was used to analyze a sequence of lithology and facies from Sambipitu formation in this study. The sedimentation pattern could be interpreted from the result of the repetition of lithology, especially in the Sambipitu formation at the Ngalang River. The repetition of lithology could determine the lithofacies that represent the depositional environment of sedimentation process. Using Markov chain analysis, the prediction of lithology or sedimentation process was determined by probability or quantitative number that must be tested in Chi-square analysis. The Markov chain analysis also implicates the recent sedimentary rocks product such as alluvial sediment or tsunami sediment are deposited.

2. Methodology

Research in this study was divided into three steps. The first step was fieldwork, followed by data analysis and report preparations, respectively (Figure 1). Primary data which was used for analysis was obtained from stratigraphic data. The stratigraphic data was collected from the Ngalang river, using a stratigraphy section measurement with a thickness of 55.9 meters. The data was gathered from observation point 1 to 6 located on the upper part of the Sambipitu formation (Figure 2). Every observation point represented different rock types or lithology variation. However, before the primary data was obtained, a preliminary analysis was conducted to collect secondary data and to produce a topography map. The fieldwork was conducted to identify the lithological properties such as colour, sedimentary structure, texture, rock composition, and fossils content.

During the second step, fossil analysis was conducted to identify planktonic and benthonic foraminifera. The analysis was carried out to determine the age and depositional environment in the research area. The determination of age was done by observing the abundance of foraminifera
in small grain size rocks samples. The determination of the age, as well as the depositional environment would support the rock distribution and rock facies. Meanwhile, the stratigraphy of the Sambipitu formation was analyzed using Markov chain model, which consist of observation of transition matrix and probability and transition matrixes. A Markov chain is a model of the random motion of an object in a discrete set of possible location (Walrand & Varaiya, 2000). In addition to the Markov chain analysis, matrix of possibility frequent transition and Chi-square analysis were also conducted. Megascopic rock name classification used was Pettijohn (1957). The classification used in facies determination was Bouma (Bouma, 1962) and Walker (Walker & James, 1992). The zone of Blow (1969) was used to determine the age and the depositional environment according to Phleger (1951) and Tipsword et al. (1966).

Figure 1. The methodology flow chart
Current morphological and rock conditions around a river can describe the past condition of the river, such as rocks formed or lithology, geological structure, current erosion and sedimentation process (Zamroni et al., 2020). Sedimentation process requires some flow current, such as turbidity current in a basin as transportation media (Selley, 1985). The Markov chain analysis can be used to assess the role of determinism ("memory") in a series of physical events (Lumsden, 1971). The value of the X factor at $t$ (time) process was named by state Hillier and
Lieberman (1995). If this system moves from state $i$ in interval time to state $j$, the system can be determined as a transition from $i$ to $j$. The possibility of transition in a step of state $i$ heading to state $j$ could be determined in a formula:

$$P_{ij} = P\{X_{tk} = j | X_{tk-1} = i\}$$ (1)

3. Result and Discussion

The measuring section at the Ngalang River consisted of six observation points, which are point 1, 2, 3, 4, 5, and 6. Every observation point represented different type of rock. Based on the result of stratigraphy section measurement, the thickness of the rock was about 55.90 meters. The rocks consisted of Calcareous Sandstone Calcarenite (Sandy Limestone), Polymics Breccia, Pebbly Sandstone, Shale, and Calcareous Siltstone. The age of the rocks was determined using foraminifera fossils identification. The age obtained was N 12 to N 14 (Middle Miocene) (Blow, 1969). The rocks were deposited at the Upper part of the Sambipitu formation and were deposited at a depth of 20 meters to 500 meters (Inner Neritic to Upper Bathyal) (Phleger, 1951) (Figure 3).

![Figure 3](image_url). The profile of tracking map of measuring section at Ngalang river

4.1 Markov chain Analysis (Lithological Pattern)

The Markov chain analysis was carried out at 44.9 meters of the measuring section along the Ngalang river in fieldwork observation. The measuring section profile was arranged at interval of 0.2 meters (20 cm) from bottom to top layers of rock distribution (Figure 4). The transition of observation matrix and the probability of transition and observation matrix showed the probability value of each rock. Data obtained from the two matrixes were then used in Markov chain analysis to show the cycle of rock repetitions related to each other.
Figure 4. The sortation of repetition rock lithology with Markov chain analysis

The probability of frequency and transition matrices in random transition matrix is probability value obtained from every lithology transition. It obtained the pattern of lithology cycle that was tested using Chi-square. By reviewing the Chi-square result, the hypotheses of random or non random rock cycle was determined. The thickness of 11 meters from the measuring section was used to compare to the presence of the next rocks using the calculation.

The Markov chain facies was also analyzed using Bouma Facies Model and Walker Facies Model (1978) based on the texture of grain size, sedimentary structures, geometric, and rock relationship. The sedimentation process was carried out by turbidity current, which created the submarine fan on submarine slopes, according to the understanding of lithology period at the Upper Sambipitu formation. The result of facies was classified with interval of 0.2 meters (20 cm) arranged from bottom to top layer based on Bouma Facies Model and Walker Facies Model (Figure 5).

Based on Bouma Facies Model, the repetition pattern of facies consists of Interval with Parallel Lamination turned to (Td) Upper Interval with Parallel Lamination (Tb) and Interval with Graded Bedding (Ta) upward. At the middle part of the section, the facies consists of Interval with Current Ripple Lamination and Convoluted Lamination (Tc) - Upper Interval With Parallel Lamination (Td) - Interval with Graded Bedding (Ta) – Lower Interval With Parallel Lamination (Tb) – Upper Interval With Parallel Lamination (Td) – Pellitic Interval (Te) – Upper Interval With Parallel Lamination (Td) – Pellitic Interval (Te). At top part, the facies consist of facies Upper Interval with Parallel Lamination (Td) - Interval with Graded Bedding (Ta) – Pellitic Interval (Te) - Upper Interval with Parallel Lamination (Td) – Pellitic Interval (Te) – Upper Interval with Parallel Lamination (Td).
Based on Bouma Facies Model, the repetition pattern of facies at the the lower part of Upper Sambipitu formation consists of Classical Turbidite (CT-2) and Clasts supported Conglomerate (CGL). At the middle part, the rock facies consists of Pebble Sandstone (PS) and Classical Turbidite (CT-1). In the upper part, the facies model was classified with Classical Turbidite (CT-1), Pebble Sandstone (PS), and Classical Turbidite (CT- model was classified with Classical Turbidite (CT-1), Pebble Sandstone (PS), and Classical Turbidite (CT-1).

### 4.2 Percentage of Probability Matrix

Based on the likelihood of lithology presence at intervals of 0.2 meters in the study field, the percentage of lithology trend was around 66.6% up to 85.71%. The predictions of lithology were
Calcareous Sandstone (A) to Calcareous Sandstone (A) (81.37%), Calcarenite (B) to Calcarenite (B) (73.61%), Shale (C) to shale (C) (66.67%), Polymics Breccia (D) to Polymics Breccia (D) (80.00%), Calcareous Siltstone (E) to Calcareous Siltstone (E) (75.00%), Pebble Sandstone (F) to Pebble Sandstone (F) (85.71%). These are the percentages of lithology presence predicted for the next 0.2 meters at a depth of 11 meters (Figure 6). Based on Markov chain, the cycles of sedimentation process are presented in Table 1.

**Table 1. Cycle of Markov chain**

| Cycle | Legend (Rock Formation) |
|-------|-------------------------|
| Cycle 1 | A (Calcareous Sandstone) – B (Calcarenite) – C (Shale) – A (Calcareous Sandstone) |
| Cycle 2 | A (Calcareous Sandstone) – B (Calcarenite) – D (Polimic Breccia) - A (Calcareous Sandstone) |
| Cycle 3 | A (Calcareous Sandstone) – B (Calcarenite) – F (Pebble Sandstone) – C (Shale) - A (Calcareous Sandstone) |
| Cycle 4 | A (Calcareous Sandstone) – B (Calcarenite) – E (Calcareous Siltstone) – C (Shale) - A (Calcareous Sandstone) |
| Cycle 5 | A (Calcareous Sandstone) – C (Shale) – B (Calcarenite) - D (Polimic Breccia) - A (Calcareous Sandstone) |
| Cycle 6 | A (Calcareous Sandstone) - D (Polimic Breccia) – B (Calcarenite) – E (Calcareous Siltstone) – C (Shale) - A (Calcareous Sandstone) |
| Cycle 7 | A (Calcareous Sandstone) - D (Polimic Breccia) – B (Calcarenite) – F (Pebble Sandstone) – C (Shale) - A (Calcareous Sandstone) |
| Cycle 8 | A (Calcareous Sandstone) – E (Calcareous Siltstone) – C (Shale) – B (Calcarenite) - D (Polimic Breccia) - A (Calcareous Sandstone) |
| Cycle 9 | A (Calcareous Sandstone) – E (Calcareous Siltstone) – B (Calcarenite) – F (Pebble Sandstone) – C (Shale) - A (Calcareous Sandstone) |

Calcareous sandstone was predicted as the type of rock that has the highest distribution percentage, which occurs at the start or end of the Markov chain cycle. The thickness of rock
distribution is also dominated by calcareous sandstone. Some variations of rock distribution show the product of sedimentation process.

### 4.3 Geological Interpretation

Geological interpretation of depositional environment in research area was determined based on the sedimentary structures, traces of fossil, benthonic foraminifera, and facies analysis model. Hummocky Cross Stratification (HCS), for example, is a sedimentary structure that can be linked to the depositional climate (HCS). Paleocurrent Analysis of HCS was obtained from the general trend of Northwest–Southeast (NW-SE). It means that the source of sedimentation comes from northwest part of the research area because the dip of a sedimentary layer is in the south direction.

Several fossils were found in the research area, such as *chondrites* (*zoophycos*), *rhizocorallium* (*cruziana* facies), and *thalasinoides* (*skolithos*) (Collinson & Thompson, 1982). By identifying the fossils trace, the depositional environments were able to be determined. The bottom part of the section was deposited on continental shelf (tidal). The middle part of the section was deposited in neritic (sub littoral), and the top part of section was deposited in upper bathyal.

Benthonic foraminifera fossils were discovered in three parts of measuring section. The bottom and the middle part of the section were identified at inner (shelf) neritic (depth of 0 - 20 meters) and the top part of the section was identified at upper slope bathyal (depth of 200 - 500 meters) (Table 2).

### Table 2. Comparison and correlation of depositional environment

| Comparison and correlation of environment depositional data before Chi-square Test | Depositional environment based on Benthonic Foraminifera | Depositional environment based on Facies |
|---|---|---|
| Top | Upper (Slope) Bathyal (depth of 200 - 500 m) | Top | Lower Fan |
| Middle | Middle (shelf) Neritic (depth of 20 - 100 meters) | Middle | Mid fan |
| Bottom | Inner (Shelf) Neritic (depth of 0 - 20 meters) | Bottom | Upper - Mid Fan |

| Comparison and correlation of environment depositional data after Chi-square Test | Depositional environment based on Benthonic Foraminifera | Depositional environment based on Facies |
|---|---|---|
| | Upper (Slope) Bathyal (depth of 200 - 500 meters) | Lower Fan |

### 4.4 Calculation of Chi-square Test

After obtaining the values of observation and expectation probability, the values were compared to the Chi-square table (Table 3) to determine the acceptance of hypotheses. Degree of freedom is $V = \{\text{total of facies} - 1\}^2 = \{4-1\}^2 = 9$. This research took a value of alpha (A) 5% with accuration rate of 5% = 0,05, so the critical value such as $\chi^2_{0.05,9} = 16.92$.

The calculation value of Chi-square distribution was 2409.86. It is higher than 16.92. It means that the null hypothesis is rejected. The null hypothesis (H$_0$) is the data derived from random transition population, the sortation of facies does not depend on previous facies. Meanwhile, the alternative hypothesis (H$_1$) is the data derived from random transition population,
the sortation of facies depends on previous facies. Based on this calculation, this implies that the significance of facies present depends on previous facies. The sortation of facies was not random and had some patterns.

### 4.5 Discussion

There were some discussions in research area related to the stratigraphy of the Sambipitu formation. The discussions will be presented in the following paragraphs.

There were some equality of probability lithology data and facies based on comparison data of lithology facies and depositional environment (Bouma facies and Walker facies). Both lithology probabilities were appropriated with facies probabilities on a thickness of 44.90 meters, but the total percentage of those probabilities was not suitable, despite the interval of Markov chain analysis being performed every 20 cm in lithology or facies.

#### Table 3. Chi-square calculation

| Class      | Observation (OJ) | Expectation (EJ) | (OJ-EJ)''/EJ |
|------------|------------------|------------------|--------------|
| CT-1 - CT-1| 136              | 90.24            | 23.20        |
| CT-1 - CT-2| 1                | 28.20            | 26.24        |
| CT-1 - PS  | 3                | 16.92            | 11.45        |
| CT-1 - CGL | 1                | 7.05             | 5.19         |
| CT-2 - CT-1| 2                | 13.20            | 9.50         |
| CT-2 - CT-2| 41               | 4.40             | 304.45       |
| CT-2 - PS  | 0                | 0.44             | 0.44         |
| CT-2 - CGL | 1                | 21.12            | 19.17        |
| PS - CT-1  | 2                | 7.80             | 4.31         |
| PS - CT-2  | 1                | 2.60             | 0.98         |
| PS - PS    | 23               | 0.26             | 1988.88      |
| PS - CGL   | 0                | 12.48            | 12.48        |
| CGL - CT-1 | 2                | 3.00             | 0.33         |
| CGL - CT-2 | 0                | 1.00             | 1.00         |
| CGL - PS   | 0                | 0.10             | 0.10         |
| CGL - CGL  | 8                | 4.80             | 2.13         |
| **Total**  | **2,409.86**     |                  |              |

#### Table 5. The comparison and correlation of facies probability data before Chi-square test on Sambipitu formation Stratigraphy with percentage of > 50 %

| Lithology                        | Bouma Facies | Walker Facies |
|----------------------------------|--------------|---------------|
| **Calcereous Sandstone -**       | **Calcereous Sandstone** | **Calcereous Sandstone** |
| **Calcereous Sandstone -**       | **Calcereous Sandstone** | **Calcereous Sandstone** |
| **Calcereous Siltstone -**       | **Calcereous Siltstone** | **Calcereous Siltstone** |
| **Calcereous Siltstone -**       | **Calcereous Siltstone** | **Calcereous Siltstone** |
| **Polymic Breccia -**            | **Polymic Breccia** | **Polymic Breccia** |
| **Polymic Breccia -**            | **Polymic Breccia** | **Polymic Breccia** |
| **Pebble Sandstone -**           | **Pebble Sandstone** | **Pebble Sandstone** |
| **Pebble Sandstone -**           | **Pebble Sandstone** | **Pebble Sandstone** |

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Based on the lithology and facies comparison data (Bouma and Walker), the Chi-square test applied to their probability facies data and revealed the same likelihood. Before the Chi-square test, there were a few different lithologies with their physical rock characteristics. There was no polimic breccia after the Chi-square was completed. It is likely that the sediment supply stopped depositing before arriving at the study area because the sediment flow was lower, resulting in the formation of fine materials at the end of the depositional phase (Table 6).

Table 6. The comparison and correlation of facies probability data after Chi-square test on Sambipitu formation Stratigraphy with Percentage of > 50 %

| Lithology                              | Bouma Facies | Walker Facies |
|----------------------------------------|--------------|---------------|
| Calcareous Sandstone - Calcareous Sandstone | 83.33%       | Tb-Tb         | CT2 - CT2 | 100 %        |
| Calcarene – Calcarene                  | 83.33%       |               |           |              |
| Calcareous Siltstone - Calcareous Siltstone | 85.71%       | Td-Td         | CT1 - CT1 | 92.22 %      |
| Pebble Sandstone - Pebble Sandstone    | 50 %         | Ta-Ta         | PS – PS   | 50 %         |
| Pebble Sandstone – Calcareous Siltstone | 50 %         | Ta-Te         |           |              |

Based on the interpretation of cross-section, the research area is located near to the source area. The percentage value of Pebble Sandstone was about 50%. Based on the cross-section, the lithology of coarse grain size decreased. This occurrence is related to the classification of turbidity deposits (Kuenen & Migliorini, 1950), which states that in the final step of depositional process, the coarse deposit location is close to the source area.

The rocks in Sambipitu formation were deposited at paleobathimetry of inner (shelf) neritic – upper (slope) bathyal based on the correlation of depositional environment. According to lithofacies review, the paleobathymetry can be translated as upper fan to lower fan (Walker & James, 1992). In this case, there was no relationship between benthonic fossil analysis and facies analysis data especially at the Upper area. The benthonic fossil analysis is upper (slope) bathyal which could not relate to facies analysis of lower fan (Walker & James, 1992).

Factors of facies distribution that cannot be linked to benthonic fossil studies are sedimentary process, supply of sediments, climate, tectonic events, the eustacy changes, and volcanic activity.

a. Sedimentary process
   Sedimentary process was affected in distribution and facies change due to progradation facies. Novian and Surjono (2011) discovered that siliciclastic sediments and carbonate materials were mixed on-site, punctuated, and mixed at the source. The facies repetition in transitional zone showed that there were some shallowing event cycles upward (middle shelf – inner shelf).

b. Supply of Sediments
   The facies thickness and types of sedimentary materials affect the sedimentary processes. The Nglanggeran Formation deposit can be used to predict the availability of sediments in
The rock product of Nglanggeran formation is the result of sedimentation, which is deposited on land and in underwater (sea). It positions a large portion of southern part of Nglanggeran Mountain in an east – west direction (Haris, 2012). Semilir Formation rocks are older than Nglanggeran Formation rocks at N4-N5 (Early Miocene) and may support the sedimentation phase in the research area (Rizqi, 2019).

c. Climate
The warm climate affects carbonates development. The bentonic fossils develop at the top part of stratigraphic measuring section where some fossils in Bathyal paleobathymetric are found. The warm climate makes a good condition of carbonate development. The presence of carbonate cement has become an indication of shallow marine with a depth of fewer than 200 meters (Donovan, 2017).

d. Tectonic events
The tectonism is a facies shift element change that is locally triggered by vertical movements and dip of a fault block. The fault in this research area, specifically located in upper part of Sambipitu formation, is controlled by sinistral fault (Putra & Pandita, 2017).

e. The eustacy (sea level) changes
The eustasy (sea level changes) caused the sea level depth to change, resulting in different sedimentary depositional products. The rocks of Sambipitu formation were deposited in intra arc basin with a shallow marine facies in the proximal facies region (Ongki et al, 2017). It was supported by the presence of andesitic lava on lower part of Sambipitu formation. The source of Sambipitu rock formation is derived from the deposition of Nglanggeran Formation, which is a part of volcanic body located under seawater. Volcanism influenced the rocks facies shift in Sambipitu and eustasy affected the upper part of Sambipitu formation (due to the sea level change).

f. Volcanism activity
Volcanism activity is caused locally by material volcanic of the Nglanggeran Formation. The presence of volcanoes and islands were the environmental factor that directly affected the depth of seawater. At the research area, the volcanic products were deposited in northern area that was included in proximal facies (Bogie, 1998).

Trace fossils presence at Ngalang River could support the interpretation of paleobathymetry or the depositional environment. Based on interpretation of the depositional environment by trace fossil identification (Seilacher, 2007), the depositional environment at bottom, middle, and top of Upper Sambipitu formation at Ngalang River is presented in Table 7. The sedimentation process occurred from continental shelf (0-20 meters) to neritic (20-100 meters). At the top part of Sambipitu formation, the sedimentation process occurred at Upper Bathyal (200 – 500 meters). It showed that the depositional environment developed from shallow marine to deeper marine related to facies model Bouma (Bouma, 1962) and Walker (Walker & James, 1992) from upper fan to lower fan (deepening upward). Purbantoro et al. (2020) who studied for detailed stratigraphy in Sambipitu revealed that Sambipitu formation deposited at Outer Neritic (20 – 100 meters) to Upper Bathyal (200-500 meters). In addition, Aprilita et al. (2020) showed the depositional system of Sambipitu formation in open circulation shallow marine based on microfacies analysis.
Table 7. The depositional environment of Upper Sambipitu formation based on trace fossil

| Trace Fossil          | Ichnofacies | Environment                        |
|-----------------------|-------------|------------------------------------|
| Top                   | (Chondrites) | Upper bathyal                      |
|                       | (Zoophycoos) | (depth of 200-500 meters)          |
|                       | (Seilacher, 2007) |                                |
| Middle                | (Rhizocorallium) | Neritic                           |
|                       | (Cruziana)   | (Sublitoral)                       |
|                       | (Seilacher, 2007) | (depth of 0-20 meters)            |
| Bottom                | Thalasinoides | Continental shelf                  |
|                       | (Skolithos)  | (Tidal)                            |
|                       | (Seilacher, 2007) | (Beach shore line)             |

4. Conclusion

The conclusion based on the analysis of stratigraphic measuring section in Ngalang River at Upper Sambipitu formation shows that the Markov chain could be used to evaluate lithology and facies using observed and measured probability transition matrix which predicted the presence of next lithology and facies. There were 9 rock cycles, in which with the highest possibility of repetition of A (Calcareous Sandstone) – B (Calcarenite) – E (Calcareous Siltstone) – C (Shale) - A (Calcareous Sandstone) is 48.60%. The presence of lithology depends on the previous lithology, in which the sortation of the lithology is not random (in a pattern). It can be seen from the result of Chi-square test with value of \( \chi^2 \text{calculation} \) (574.40) > \( \chi^2 \text{table} \) (37.65). The lithology prediction of the next 0.2 meters were calcareous sandstone to Calcareous sandstone, Calcarenite to Calcarenite, Pebble Sandstone to Pebble Sandstone, Calcareous siltstone to calcareous siltstone.

The sortation of stratigraphic measuring section (Bouma, 1962) on the upper part of Sambipitu formation with the strongest possibility is Ta (Interval With Graded Bedding) or and Tc (Interval With Current Ripple Lamination and Convolute Lamination) or and Td (Upper Interval With Parallel Lamination) or and Ta (Interval With Graded Bedding) about 40%. The rock facies prediction (Bouma, 1962) is based on the previous facies which the rock facies was not random (in a rock pattern). It can be seen from the Chi-square test with value of \( \chi^2 \) (605.65) is more than \( \chi^2_{0.05;9} \) (26.30).
The prediction of facies that will be found (Bouma, 1962) of the next 0.2 meters are (Tb) Lower Interval with Parallel Lamination to (Tb) Lower Interval with Parallel Lamination, (Td) Upper Interval with Parallel Lamination to (Td) Upper Interval with Parallel Lamination, (Te) Pellitic Interval to (Te) Pellitic Interval. The facies sortation (Walker & James, 1992) on the upper part of Sambipitu formation showed that the biggest possibility of repetition pattern is (CT-1 Classical Turbidite) to (PS Pebbly Sandstone) to (CT-2 Classical Turbidite) to (CGL Clast Supported Conglomerate) to (CT-1 Classical Turbidite) about 28.25%. The presence of rock facies (Walker & James, 1992) depend on the previous facies which the sortation of facies is not random. This can be seen from the Chi-square test result with value of $\chi^2$ (2409.86) is more than $\chi^2_{0.059}$ (16.92). The prediction of facies presence (Walker & James, 1992) of the next 0.2 meters are (CT-1 Classical Turbidite) to (CT-1 Classical Turbidite), (CT-2 Classical Turbidite) to (CT-2 Classical Turbidite), and (PS Pebbly Sandstone) to (PS Pebbly Sandstone).

The next or future research could be done on rock contact formation in between Sambipitu and Oyo Formation by using Markov chain analysis. Sedimentary structure analysis is required to make a comprehensive interpretation of geological data.

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**References**
Apriani, A. (2016). Metode Markov chains Untuk Analisa Perulangan Fasies Di Sub Basin Kiliran Jao Sumatra Barat. *Angkasa: Jurnal Ilmiah Bidang Teknologi*, VIII(1), 1–16. https://doi.org/10.28989/angkasa.v8i1.128

Aprilita, L., Pandita, H., & Nuraini, S. (2020). Analisis Fasies pada kontak antar formasi Sambipitu dan formasi Oyo di lintasan kali Ngalong, Gunungkidul. *Geoda2, I*(2), 43–52.

Blow, W. H. (1969). Late Middle Eocene to Recent planktonic foraminiferal biostratigraphy. In E. Brill (Ed.), *Proceedings of the First International Conference Planktonic Microfossils 1967* (Vol. 1, pp. 199-242).

Bogie, I. (1998). The application of a volcanic facies model to an andesitic stratovolcano hosted geothermal system at Wayang Windu, Java, Indonesia. *Proceedings of 20th NZ Geothermal Workshop*.

Bothe, A. C. D. (1929). The Geology of the Hills Near Djowo and Southern Range. *4th Pacific Science Congress*.

Bouma, A. H. (1962). *Sedimentology of Some Flysch Deposits: A Graphic Approach to Facies Interpretation*. Elsevier.

Collinson, J. D., & Thompson, D. B. (1982). *Sedimentary Structures*. Allen at Unwin Publishers Ltd.

Dicky Candrawan Putra, & Pandita, H. (2017). Identification of Kali Ngalong fault in Karanganyar village, Ngalong, Gedang Sari Sub district, Gunungkidul Regency, Special Regency of Yogyakarta. *Prosiding Nasional Rekayasa Teknologi Industri Dan Informasi XIV Tahun 2019 (ReTII)*, 1–11.

Donovan, S. K. (2017). Trace fossils and tropical karst. *Geological Magazine*, 154(1), 166–168. https://doi.org/10.1017/S0016756815000965

Haris, F. (2012). *Geologi dan studi Formasi Nglanggeran Daerah Patuk dan sekitarnya, Kecamatan Patuk, Kabupaten Gunungkidul, Provinsi D.I. Yogyakarta*. UPN Veteran.

He, J., La Croix, A. D., Wang, J., Ding, W., & Underschultz, J. R. (2019). Using neural networks and the Markov chain approach for facies analysis and prediction from well logs in the Precipice Sandstone and Evergreen Formation, Surat Basin, Australia. *Marine and Petroleum Geology*, 101, 410–427. https://doi.org/10.1016/j.marpetgeo.2018.12.022

Hillier, F. S., & Lieberman, G. J. (1995). *Introduction to Operations Research, Sixth Edition*. McGraw-Hill.

Jun, H., Cho, Y., & Noh, J. (2019). Trans-dimensional Markov chain Monte Carlo inversion of sound speed and
temperature: Application to Yellow Sea multichannel seismic data. *Journal of Marine Systems, 197*, 103180. https://doi.org/https://doi.org/10.1016/j.jmarsys.2019.05.006

Kuenen, P. H., & Migliorini, C. I. (1950). Turbidity Currents as a Cause of Graded Bedding. *The Journal of Geology, 58*(2), 91–127. https://doi.org/https://doi.org/10.1086/625710

Lumsden, D. N. (1971). Markov chain analysis of carbonate rocks: applications, limitations, and implications as exemplified by the Pennsylvania system in southern Nevada. *Geological Society of America Bulletin, 82*(2), 447–462. https://doi.org/https://doi.org/10.1130/0016-7606(1971)82<447:MCAOCR>2.0.CO;2

Michael, H. A., Li, H., Boucher, A., Sun, T., Caers, J., & Gorelick, S. M. (2010). Combining geologic-process models and geostatistics for conditional simulation of 3-D subsurface heterogeneity. *Water Resources Research, 46*(5), W0552. https://doi.org/https://doi.org/10.1029/2009WR008414

Novian, M. I., & Surjono, S. S. (2011). *Stratigrafi dan sedimentasi zona transisi formasi Sambipitu: Formasi Oyo jalur Kali Widoro, Ngalong dan Kedungdowo, Kecamatan Nglipar, Kabupaten Gunungkidul, Daerah Istimewa Yogyakarta*. Universitas Gadjah Mada.

Pandita, H. (2008). Depositional environment of Sambipitu formation Based on Trace Fossil in Nglipar Area. *JTM, Institut Teknologi Bandung, XV*(2), 85–94.

Pettijohn, F. J. (1957). *Sedimentary Rocks*. Herper.

Phleger, F. B. (1951). *Ecology of Foraminifera, Northwest Gulf of Mexico*. The Geological Society of America.

Pramunita, S. W., & Pandita, H. (2020). Analisis kepadatan fosil jejak sebagai parameter tingkat kandungan oksigen dan perubahan lingkungan pengendapan di Kali Ngalong, Gedangsari, Gunungkidul, DIY. *Geoda, 1*(2), 1–18.

Purbantoro, R., Rizqi, A. H. F., & Nuraini, S. (2020). Konfigurasi stratigrafi batas formasi Sambipitu dan oyo di Jalan Ngalong –Gading, Kecamatan Gedangsari–Playen, Gunungkidul. *Geoda, 1*(2), 81–94.

Rizqi, A. H. F., & Purnomo, H. T. (2019). Analisis Siklus Perulangan Litologi pada Formasi Sambipitu. *Prosiding Nasional Rekayasa Teknologi Industri Dan Informasi XIV Tahun 2019 (ReTII), November*, 359–375.

Seilacher, A. (2007). *Trace Fossil Analysis*. Springer-Verlag Berlin Heidelberg.

Selley, R. C. (1985). *Ancient Sedimentary Environments, 3rd edition*. Cornell University Press.

Suprapto, N., Zamroni, A., & Yudianto, E. A. (2017). One Decade of the “LUSI” Mud Volcano: Physical, Chemical, and Geological Dimensions. *Chemistry, 26*(4), 615–629.

Surono, Toha, B., Sudarno, I., & Wiryosujono, S. (1992). *Stratigraphy of Southern Mountain, Central Java*. P3G-Ditjen GSM Dept. Pertamben.

Tipsword, H. L., Setzer, F. M., & Smith Jr, F. L. (1966). Interpretation of Depositional Environment in Gulf Coast Petroleum Exploration from Paleoecology and Related Stratigraphy. *Gulf Coast Association of Geological Societies Transactions, 16*, 119–130.

van Bemmelen, R. W. (1949). General Geology of Indonesia and adjacent archipelagoes. In *The geology of Indonesia*. The Hague, Martinus Nijhoff.

Walker, R. G., & James, N. P. (1992). *Facies Models: Response to sea Level Change*. Geological Association of Canada.

Walrand, J., & Varaiya, P. P. (2000). *High-performance Communication Networks* (Second Edi). Morgan Kaufman Publishers.

Zamroni, A., Putra, B. P., & Prasetya, H. N. E. (2020). Anthropogenic influences on morphological changes in the Progo River, Daerah Istimewa Yogyakarta Province, Indonesia. *Sustinere: Journal of Environment and Sustainability, 4*(3), 205–223. https://doi.org/https://doi.org/10.22515/sustinere.jes.v4i3.119