Wear of micro diamond tool in ultra-precision turning under dry and minimum quantity lubrication conditions

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Abstract
Minimum quantity lubrication (MQL) is an effective way to reduce the cutting temperature and tool wear. To reveal the effect of MQL on the wear of micro diamond tool, a calculation model for the cutting temperature of micro diamond tool under dry friction condition is established firstly by using the Fourier’s law of heat conduction. Regarding the boundary film as a layer of heat-conduction medium, a revised calculation model for the temperature distribution on tool rake face under MQL condition with different cutting fluids is further established. The predicted results indicate that low viscosity is beneficial to the wetting of cutting fluid on tool-chip contact interface, which can relieve the friction. The reduction of friction finally decreases the cutting temperature. Secondly, the cutting temperature–dependent wear volume of micro diamond tool is predicted by using the Usui wear rate model in response to different cutting fluids and different cutting distances. In dry cutting, the graphite wear of micro diamond tool prevails. However, the application of MQL can slow down the graphitization of diamond, so the wear of micro diamond tool visibly decreases. Finally, cutting experiments with different cutting fluids are performed to verify the established models. The experimental observations agree well with the theoretical prediction results. Such satisfactory consistency confirms that the cutting fluid with low viscosity can reduce the cutting temperature and inhibit tool wear effectively.

Keywords
Minimum quantity lubrication · Micro diamond tool · Cutting temperature · Cutting fluid

1 Introduction
Micro-cutting technology is usually used for manufacturing small-size parts, in which micro diamond tools are indispensable. In this work, micro diamond tools refer to the diamond tools with a nose radius of less than 100 μm. Due to the small nose radius, the preparation of micro diamond tools is much more difficult than the conventional diamond tools, which requires higher precision machine tools for sharpening. Especially for the tool with micro nose radius of less than 30 μm, the sharpening process is required to be quite stable. This is because small changes of sharpening parameters may produce large profile errors on the cutting edge [1]. With the development of micro-nano manufacturing technology, high-efficiency and low-cost processing have become the urgent requirement in different industrial sectors.

Therefore, more rigorous wear resistance is put forward for the micro diamond tools. As well known in micro-cutting, the depth of cut and feed rate are extremely small, which will introduce the size effect and increase the cutting ratio significantly. Meanwhile, a large amount of heat flux will be generated, which eventually increases the temperature of the tool itself due to its small heat capacity. An elevated cutting temperature inevitably accelerates tool wear. Therefore, in micro-cutting, the excellent wear resistance, thermal hardness, impact resistance, and other aspects of the tool are necessary.

Micro-cutting is a complex plastic deformation process, and deformation generates cutting force and cutting heat. In the cutting process, the plastic deformation of chips, tool-chip friction, and elastic recovery of workpiece surface will all cause the increase of cutting temperature. When the cutting temperature rises to the internal bond energy of diamond, it will lead to the fracture of carbon–carbon bond, causing the wear of cutting edge, which affects the life of micro diamond tool. In addition, the wear of tool further increases the cutting force, elastic recovery, chip
deformation, and cutting temperature, which in turn promotes the increment of tool wear. Therefore, the amount of cutting heat flux and cutting heat distribution, especially the conduction of cutting heat in the tool, is always the hot issues in micro-cutting. In fact, cutting heat has a great influence on the tool wear rate, surface accuracy of workpiece, and the surface integrity of microstructure. Therefore, the research on cutting heat is of great significance for micro-cutting technology.

Up to now, there are three methods to model the cutting heat, i.e., analytical modeling [2], digital modeling [3], and hybrid modeling [4]. Analytical modeling is to find the relationship between various variables and establish the corresponding mathematical model. Digital modeling depends on the finite element simulation. With the increasing accuracy of material constitutive models, the digital modeling method has been applied more and more, which can direct the actual machining. Hybrid modeling is a combination method of analytical and digital modeling.

Komanduri and Hou provided a comprehensive review of recent advances in cutting temperature measurement methods and claimed that the accurate prediction of cutting temperature field and thermal distribution remains a major challenge. This is because the cutting temperature measurement during machining is very difficult, which is a challenge for any model validation [5]. Abukhshim et al. concluded that as the cutting velocity increases, the heat transferred to the tool increases due to the increased contact area between the tool and the chip. In terms of their experimental observations, the percentage of cutting heat transferred to the tool will reach 65% at a cutting velocity of 1200 m/min [6]. In order to predict the cutting temperature distribution on tool rake and flank faces, Grzesik et al. used a special algorithm of the finite difference method and the method of elementary balance (MEB) to analyze the temperature in machining of C45 carbon steel with uncoated and coated ISO P20 carbide tools at a cutting velocity of 72–145 m/min, which yielded a good prediction accuracy (6%) [7].

Wang et al. determined the heat distribution ratio according to the lengths of adhesion zone and sliding zone, and finally established a temperature prediction model with consideration of non-uniform heat intensity distribution at the tool-chip contact interface [8]. Sawangsri and Cheng concluded that in micro-cutting of aluminum alloy, the ratio of cutting heat distributed in the tool, tip area, and workpiece is 8:8.5:1. In cutting of single crystal silicon, however, the cutting heat distribution ratio is 14:16:1. For the titanium alloy, the ratio of cutting heat distributed in the tool, tip, chip, and workpiece becomes 350:460:1.4:1 [9]. Davies et al. compared the measured temperature with the finite element method predicted temperature and found large difference in the results acquired by these two methods. They concluded that such difference is caused by two reasons, i.e., the error of modeling method and the error of non-deterministic factors in experiment [10]. Zhao and Liu [11] explored the effect of AlTiN coating on the cutting heat distribution coefficient and cutting temperature increment in orthogonal cutting of Inconel 718.

Finite element method (FEM) is effective in predicting the distribution of cutting temperature. Puls et al. developed a FEM-based simulation model to analyze the heat distribution in dry metal cutting [12]. You and Lee employed the Taguchi method to determine the factors affecting the turning process. They found that in machining of titanium alloys, the reason of tool wear is chip adhesion dependent on the high cutting temperature [13]. Hao et al. carried out a lot of friction tests at high temperature to emulate the hard machining of H13 hardened steel by using TiAlN-coated tool and uncoated tool, respectively [14]. Su et al. discussed on the variations of cutting temperature, tool-to-cutting chip contact temperature, and tool-to-workpiece contact temperature with tool temperature in light of tool wear and surface integrity [15]. Meng and Lin developed a 2D FEM orthogonal cutting model for the analysis of high-speed milling of ADC12 aluminum alloy [16]. Karaguzel and Budak presented a new approach for modeling and measuring the change of tool temperature in milling. This new model can predict the effect of milling conditions on the cutting temperature and, in particular, determine the relationship between the tool temperature and the depth of cut [17]. The above articles all concentrated on the modeling of cutting temperature field under dry cutting condition. There is no research to compare the temperature field under different cutting fluids and reveal the inhibiting effect of different cutting fluids on the wear of diamond tool.

However, the factors affecting the cooling effect of lubrication had been discussed, such as the nozzle angle, droplet size, evaporation rate, and others. For instance, Kulkarni et al. [18] tested three kinds of coolant supply methods, namely, dry, MQL, and nano-fluid MQL, in which the nozzle angles were set to 25° and 50°. They found that the best cooling nozzle angle is 25°. In order to evenly spray the coolant onto the tool-chip contact interface, Saha et al. [19] developed a model to analyze the characteristics of MQL jet and oil droplet, in which the cutting edge shape of the micro-end milling cutter and the elastic recovery rate of the workpiece material affecting the contact area of tool-workpiece interface were considered. By using a fixed nozzle angle, they further discussed the interaction between the oil droplets and the micro-end milling tool at different rotating speeds. Elanchezian and Kumar [20] carried out many grinding experiments on the Ti-6Al-4 V substrate by spraying the low-temperature carbon dioxide (CO₂) and conventional coolant, respectively. They investigated the effects of nozzle angle and depth of cut on the surface roughness under low-temperature CO₂ and concluded that the best
surface quality of the workpiece was achieved by using a nozzle angle of 45°. In order to improve the machinability of the hardened material, Gajrnai et al. [21] performed cutting experiments to optimize the MQL parameters, including the cutting fluid composition and nozzle angle. Their experiment results demonstrated that a nozzle angle of 45° produces the minimal cutting force.

Nanoparticle-enhanced micro-lubrication technology has been widely used in green cutting. For this new lubrication technology, nanoparticles of specific material are usually added into the lubricant. It has been found that the added nanoparticles can significantly improve the thermal conductivity, permeability, and wear-reducing and anti-wear properties of lubricants [22, 23]. The cutting fluid with different nanoparticles as added will present different cooling and lubrication effects. Wu et al. [24] found that the lubricating oil mixed with copper oxide, titanium dioxide, or diamond nanoparticles shows the excellent anti-wear performance, among which the copper oxide nanoparticles yield the best performance. Based on a lot of milling tests, Nguyen et al. [25] discovered that the lubrication of the vegetable oil mixed with the hexagonal boron nitride (hBN) nanosheets is obviously better than that mixed with the exfoliated graphite nanosheet (xGNP). Lee and Lee [26] claimed that there are slight differences in the lubricating property between the nano-diamond and nano-Al$_2$O$_3$ particles. However, the nano-Al$_2$O$_3$ particles have a superior access to reduce the achieved surface roughness. Through the ball-to-disk friction and wear tests, Luan and Qian [27] concluded that the nano-ZnO-modified fluid has better effect than the nano-Al$_2$O$_3$ mixed fluid on reducing the friction coefficient and surface wear. In addition to nanofluids, degradable lubricants such as vegetable oils are also widely used in MQL. Dhar et al. [28] investigated the effect of MQL on tool wear and surface roughness when turning AISI-4340 steel with carbide inserts. The results show that MQL can effectively reduce the cutting surface roughness. Zhang et al. [29] used numerical control precision surface grinder for surface grinding of 45 steel workpiece and used MQL lubrication method for cutting lubrication and cooling. The lubricating properties of soybean oil, palm oil, and rapeseed oil as lubricating oils were discussed. Zhang et al. [30] studied tool wear and cutting forces when milling Inconel 718 under different cutting conditions (dry cutting and MQL with degradable vegetable oil as lubricant). Nanoparticle-enhanced micro-lubrication technology is one of the most commonly used green lubrication methods at present, but it has not been applied in the field of ultra-precision machining because the nanoparticles can scratch the machined surface. According to the above reasons, this paper mainly studies the effect of alkane cutting fluid on diamond tool wear inhibition. Most of the above research work focuses on the corresponding relationship between workpiece surface morphology and cutting fluid, and most of them are in the field of conventional cutting. There is no specific research on the effect of different cutting fluids on inhibiting diamond tool wear in the field of ultra-precision machining, so this paper takes this as the core content to explore the inhibition effect of different viscosity cutting fluids on diamond tool wear in MQL.

This work aims to develop the suppression method for the wear of micro diamond tools from the perspective of reducing cutting heat and improving tool strength. Firstly, the wear mechanism of micro diamond tools in cutting of 6061 aluminum alloy is explored. Secondly, the models to predict the temperature distribution of tool under dry friction and MQL conditions are established respectively. As expected, the highest temperatures of tool under dry friction and different cutting fluids are calculated, which is used to select the best cutting fluid for the suppression of tool wear.

2 Theoretical model of cutting temperature

2.1 Generation of cutting heat

In micro-cutting, the wear of diamond tool is usually resulted from the cutting heat and cutting force, which are complementary with each other. For instance, when diamond tool with a large nose radius more than 100 $\mu$m cuts aluminum alloy, the cutting edge mainly suffers from the micro-crack wear and thermochemical wear caused by the cutting heat and cutting force. Unfortunately, there is a lack of research on the mechanism of cutting heat generation when using micro diamond tool. Previous studies revealed that during micro-cutting, different workpiece materials, different cutting velocities, and different tool parameters will change the amount of cutting heat as generated.

The workpiece materials undergo shear deformation and elastic–plastic deformation under the cutting action of micro diamond tool, resulting in the deformation resistance force, i.e., cutting force. The cutting force produces deformation work, and the deformation work generates cutting heat. In addition, the friction between the tool rake face and the chip surface and the friction between the tool flank face and the machined surface will also generate heat. Therefore, there are three heat sources in response to the three deformation zones in the cutting process, as shown in Fig. 1. The first source is the shear deformation appearing in the primary deformation zone. The second source is the friction heat due to the contact between the rake face and the chip in the secondary deformation zone. The third source is also the friction heat due to the contact between the flank face and the machined surface in the tertiary deformation zone.
2.2 Modeling on the cutting heat

As illustrated in Fig. 1, three deformation zones jointly generate the cutting heat. In dry cutting, the cutting heat mainly distributes in the chip, workpiece, and tool. Here, the heat fluxes in the chip, workpiece, and tool are denoted as $Q_C$, $Q_W$, and $Q_T$, respectively. Since the heat flux generated in the third deformation zone is tiny and can be ignored, the total heat flux $E_Q$ is formulated as

$$E_Q = Q_C + Q_W$$  \hspace{1cm} (1)

For the heat flux in the chip, heat generated in the first deformation zone $Q_C$ is calculated as

$$Q_C = F_c \cdot v_c$$

where $v_c$ is the shear velocity in the first deformation zone, and $F_c$ is the shear force in the first deformation zone.

$F_c$ is written as

$$F_c = d_u \int_0^t \tau_x dx$$

where $\tau_x$ is the shear stress, $A_x$ is the shear area.

Likewise, $Q_W$ is given by

$$Q_W = F_f \cdot v_{sh}$$

where $v_{sh}$ is the relative velocity between the chip and tool. $F_f$ is the friction force in the second deformation zone.

$F_f$ is expressed as

$$F_f = \left(1 - 2^{-a} + \frac{2^{a+1} - 1}{2^{a(a+1)}}\right) \cdot \mu \cdot \sigma_{sz} \cdot \frac{\cos(\alpha_r - \phi) \cdot t_u \cdot d_u}{\sin \phi}$$  \hspace{1cm} (2)

where $a$ is the power index, $\mu$ is the coefficient of friction. $\alpha_r$ is the effective rake angle of micro diamond tool. $\phi$ is the shear angle. $t_u$ is the depth of cut. $d_u$ is the cutting width.

The heat generated in the first and second deformation zones will change the temperature distribution. The temperature rise in the first deformation zone caused by the shear deformation is empirically calculated as [31]

$$\theta_s = \frac{\tau_x}{c_w \cdot \rho_w \cdot \tan \phi} \cdot \text{erf} \left(\frac{R \cdot \tan \phi}{4}\right)$$  \hspace{1cm} (3)

where erf is the error function.

In Eq. (3), the expression of $R$ is

$$R = \frac{c_w \cdot \rho_w \cdot v_c \cdot h}{k_w}$$  \hspace{1cm} (4)

where $k_w$ is the thermal conductivity of workpiece. $c_w$ is the heat capacity per unit volume. $\rho_w$ is the density of workpiece. $h$ is the undeformed chip thickness. $v_c$ is the cutting velocity.

The temperature distributed in the second deformation zone is affected by the plastic deformation in the first deformation zone and the friction effect between the tool and the chip. The heat from the second deformation zone is transferred into the micro diamond tool from the rake face, and the conduction pattern of which is in accordance with the Fourier’s law. In this work, the Fourier heat transfer law is the theoretical basis to determine the temperature field in the second deformation zone or inside the tool.

2.3 Modeling on the cutting temperature field under different conditions

Minimum quantity lubrication (MQL) technology is a promising cooling and lubrication method in metal cutting. In this work, such cooling and lubrication method was also used to suppress tool wear. Under the condition of MQL, the contact state between the tool and the chip can be divided into two types, i.e., boundary film contact and no boundary film contact [32]. Under the influence of boundary film contact state, the friction coefficient at the tool-chip interface changes, resulting in a reduction in friction, which in turn leads to the variation of temperature field in the cutting area or inside the tool. Therefore, the establishment of cutting temperature field under the boundary film condition is very important for exploring the best method to suppress tool wear. Up to now, little models of the cutting temperature field under MQL have been reported. Therefore, in this work, the cutting temperature field models under dry cutting and boundary film...
conditions were established according to the Fourier’s law of heat conduction.

### 2.3.1 Dry cutting condition

For the dry cutting mode, no lubrication is used. In this condition, the chip and tool rake face contact directly, and the friction heat is transferred into the tool from the rake face. Moreover, the cutting heat generated in the first deformation zone will also be transferred into the tool by conduction. According to the Fourier law of heat conduction and based on the relationship between tool cutting temperature and wear volume to be established in this paper, three assumptions should be made before establishing the cutting temperature model. Firstly, the generation and distribution of heat sources are in a steady-state. Secondly, all the energy generated in the second deformation zone is converted into heat, ignoring the energy used for phase change within the material. Thirdly, as the maximum temperature is considered in this paper, the friction heat from the second deformation zone is assumed to be the maximal temperature dependent on the friction heat from the second deformation zone.

The heat flux per unit area of the second deformation zone is expressed as

$$q_0 = F_f \cdot V_{sh}/A_{sh}$$  \hspace{1cm} (5)

where $F_f$ is the friction force of tool-chip in dry cutting, $V_{sh}$ is the sliding velocity of chip relative to the rake face, $A_{sh}$ is the tool-chip contact area.

The nose radius of micro diamond tools is usually no more than 100 μm, which is far less than the diamond thickness of tool. Therefore, a one-dimensional heat transfer model is proposed to represent the heat transfer state of the tool in light of the Fourier law of heat conduction, when the micro diamond tool is in the state of dry friction, the one-dimensional heat transfer function can be formulated as

$$\frac{\partial \theta}{\partial t} - \psi_s^\frac{\partial^2 \theta}{\partial x^2} = 0$$  \hspace{1cm} (6)

where $\psi_s$ is the thermal diffusivity of tool material (diamond).

As Eq. (6) involves time variables, it can be solved using the Laplace transform. Supposed that the diamond thickness of tool is $l$ and the original temperature of tool is 20 °C, the boundary condition of the partial differential equation is

$$\begin{align*}
\left. \frac{\partial \theta}{\partial x} \right|_{x=0} &= -\frac{q_0}{k_s} \\
\theta(l, t) &= 20
\end{align*}$$  \hspace{1cm} (7)

where $k_s$ is the tool’s thermal conductivity.

To improve the accuracy of the model, the Laplace transformation is employed to obtain the analytical solution of Eq. (7). Regarding $x$ as a parameter and performing the Laplace transformation for the independent variables $t$ on both sides of Eq. (7) can yield

$$L(\theta(x, t)) = ^\wedge \psi_s \theta(x, p)$$  \hspace{1cm} (8)

where $L$ is the Laplace transform, and $x$ is the distance, assuming $p$ as a constant.

The Laplace transformation is also performed on the boundary conditions, which produces the following ordinary differential equation:

$$^\wedge \theta_{xx}(x) = \frac{1}{\psi_s} \ ^\wedge \theta(x, p)$$  \hspace{1cm} (9)

The definite solution problem of Eq. (7) can be solved. The general solution is given by

$$^\wedge \theta(x, p) = c_1(p)e^{\sqrt{p}\psi_s x} + c_2(p)e^{-\sqrt{p} \psi_s x}$$  \hspace{1cm} (10)

Equation (10) can be simplified as

$$^\wedge \theta(x, p) = g(p) \cdot e^{-\sqrt{p} \psi_s x}$$  \hspace{1cm} (11)

Regarding $x$ as a parameter and calculating convolution on both sides of Eq. (11) can output the Laplace inverse transformation, i.e.,

$$L^{-1}[e^{-\sqrt{p} \psi_s x}] = \frac{X \cdot 2^n \sqrt{\psi_s}}{2 \sqrt{\pi} \cdot r^{3/2} \cdot e^{-\frac{x^2}{4 \psi_s r}}}$$  \hspace{1cm} (12)

Therefore, the temperature distribution on the rake face due to the friction heat from the second deformation zone is calculated as

$$\theta_s(x, t) = \theta_0 - \frac{q_0}{k_s} \cdot \sum_{i=1}^{n} (-1)^{i} \cdot \text{erfc} \left( \frac{i \cdot 2^n + x}{2 \sqrt{\psi_s r}} \right) + \theta_0 - \frac{q_0}{k_s} \cdot \sum_{i=1}^{n} (-1)^{i} \cdot \text{erfc} \left( \frac{i \cdot 2^n - x}{2 \sqrt{\psi_s r}} \right)$$  \hspace{1cm} (13)

where $l$ is the length of contact between the rake face of the tool and the chip.

The temperature distributed on the rake face is related to not only the friction heat in the second deformation zone, but also the shear deformation in the first deformation zone. Therefore, the maximum temperature on the rake face can be modified as

$$\theta_{\max} = \theta_{\max} + \theta_{st} + \theta_0$$  \hspace{1cm} (14)

where $\theta_{\max}$ is the maximal temperature dependent on the friction heat in the second deformation zone. $\theta_{st}$ is the temperature rise in the second deformation zone caused by the plastic deformation in the first deformation zone. $\theta_0$ is the ambient temperature.

### 2.3.2 Boundary film lubrication

MQL is a green lubrication method and has some unmatched advantages, such as low energy consumption, low cost, and less...
environmental pollution [33]. It has become the preferred cooling method in the cutting operation. The specific structure of the MQL unit is shown in Fig. 2. The MQL unit supplies the cutting fluid to the cutting area as water droplets with a tiny radius. The micro-defects on the surfaces of tool and chip form capillary tubes, through which the cutting fluid is brought to the tool-chip contact area by capillary action. The lubricant forms a boundary film between the tool and chip, which serves to reduce the coefficient of friction and can be thought of as a layer of medium for heat transfer. Due to the limited amount of lubricant sprayed, the oil film does not fill the entire tool-chip contact surface. Therefore, under MQL condition, the cutting fluid does not act on the entire tool-chip contact area, which will be divided into two parts, i.e., dry friction and boundary lubrication regions. We will model the heat transfer for the boundary film and dry friction cases separately, and then weight the average according to the proportion of both, followed by the lubricant with the better temperature reduction effect. First, we have to obtain the proportion of the boundary film situation on the tool-chip contact surface. According to previous work [34], the ratio of boundary lubrication area to total contact area is given by

$$\beta = e^{-\frac{x}{t_x}}$$

where $t_x$ is the cutting velocity $v$ dependent time over a distance of $x$, and $t_x = x/v$. $t_x$ is the average time that the adsorbed molecules stay on the surface.

$t_x$ is expressed as

$$t_x = t_0 \cdot e^{-\left(\frac{x}{k_0}\right)}$$

where $t_0$ is the thermal vibration period of the adsorbed molecules, and the direction of which is perpendicular to the processing surface. $k_0$ is the heat of adsorption. $R$ is a constant, and $R = 8.314 \text{ J/mol·K}$. $T_s$ is the temperature on tool surface during dry friction.

As discussed above, the actual tool-chip contact surface can be divided into dry friction and boundary lubrication regions under MQL condition. Due to the different conduction media, the cutting heat transfer in these two regions is different. Therefore, only the temperature in the second deformation zone under lubrication condition with boundary film will be discussed in this work.

In the state of boundary lubrication, an oil film will be formed between the rake face and the chip. Due to the effect of lubricating oil, the friction coefficient between the rake face and the chip is reduced, which relieves the tool-chip friction and suppresses the generation of cutting heat. In addition, heat is transferred into the tool by both heat conduction and heat convection due to the temperature gradient in the cutting fluid. However, in the field of MQL, conventional lubricants (excluding nanofluids) remove very little heat through thermal convection [35]. In order to simplify the modeling process, the heat flow carried away by the thermal convection is negligible in this work. Therefore, the oil film will be treated as a layer of heat conduction medium. Moreover, it should be further assumed that the heat flux only propagates along with the thickness of the boundary film, and the thickness of the boundary film is equal everywhere. Finally, the Fourier heat conduction equation under the boundary film state is constructed as

$$\psi_c \frac{\partial^2 \theta_1}{\partial x^2} = \frac{\partial \theta_1}{\partial t}$$

$$\psi_s \frac{\partial^2 \theta_2}{\partial x^2} = \frac{\partial \theta_2}{\partial t}$$

where $\psi_c$ is the thermal diffusivity of lubrication oil. $t$ is the time.

The boundary conditions for the contact between the oil film and the chip are given by

$$k_c \frac{\partial \theta_1}{\partial x} = -q_1 \quad x = 0, \quad t \geq 0$$

$$\theta_2(x, t) = 0 \quad x \to \infty, \quad t \geq 0$$

where $q_1$ is the heat flux per unit area generated by the friction force on the tool-chip interface under the boundary...
lubrication conditions; \( k_c \) is the lubrication oil’s thermal conductivity.

Similarly, the boundary conditions for the oil film and tool contact are written as

\[
\theta_1(x_1, t) = \theta_2(x_1, t)
\]

\[
-k_c \frac{\partial \theta_1}{\partial x} \bigg|_{x=x_1} = -k_s \frac{\partial \theta_2}{\partial x} \bigg|_{x=x_1}
\]

Finally, the Laplace transformation is performed for the time variable \( t \), and the Fourier transformation is carried out for the position variable \( x \), through which the above partial differential equations can be used to solve the temperature distribution on tool rake face under the boundary lubrication conditions, i.e.,

\[
\theta = q_1 \cdot \frac{4 \sqrt{k_c}}{\psi_c \cdot k_c} \sum_{n=0}^{\infty} (|d|)^{n+1} \cdot \sqrt{1 \cdot \pi} \cdot \left\{ \exp \left[ -\frac{(n+1)^2 \cdot x_1^2 \cdot \psi_c}{t} \right] - \text{erfc} \left[ \frac{(n+1) x_1 \sqrt{\psi_c}}{\sqrt{t}} \right] \right\} + \frac{2q_1}{k_c} \sqrt{\frac{t}{\pi \cdot \psi_c}}
\]

\[
d = k_c \cdot \psi_c \sqrt{\psi_s} - k_s \cdot \psi_s \sqrt{\psi_c}
\]

\[
q_1 \text{ is expressed as}
\]

\[
q_1 = F_f \cdot V_{sh} / A_{sh}
\]

where \( F_f \) varies with different lubricants.

The calculated results of temperature rise on tool rake face under different contact conditions are presented in Fig. 3. It can be found that under the same cutting parameters, the highest temperature on tool rake face under the boundary lubrication condition is significantly smaller than that achieved under the dry friction condition, which shows that the MQL technology has a good effect on reducing the cutting heat.

To simplify the temperature model, it is assumed that the average temperature of tool-chip contact region in response to the boundary lubrication condition is \( \theta \), and the average temperature of tool-chip contact region in response to the dry friction condition is \( \theta_m \). In terms of the reported finding [36], the boundary film discretely distributes on the rake face, so the Maxwell-Oaken model is used to calculate the temperature superimposition of the boundary lubrication and dry friction contact regions. With consideration of the coupling effect of dry friction and boundary film, the average temperature \( \bar{\theta} \) of the rake face can be expressed as

\[
\bar{\theta} = \frac{(1 - \beta) \cdot (2 - \beta) \cdot \theta_m + \beta \cdot (3 - 3 \cdot \beta) \cdot \theta}{2 - 2 \cdot \beta^2}
\]

Because of \( 0 < \beta < 1 \), Eq. (26) reveals that the temperature of tool rake face under the boundary lubrication condition is significantly lower than the temperature under the dry friction condition, namely \( \theta < \theta_m \). Therefore, the following relationship is fulfilled:

\[
\beta \cdot (3 - 3 \cdot \beta) \cdot \theta < \beta \cdot (3 - 3 \cdot \beta) \cdot \theta_m
\]

Equation (27) confirms that the temperature of micro diamond tool can be effectively reduced by using the MQL technology.

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Fig. 3 Tool temperature rise as calculated under different contact conditions. a dry friction condition b boundary lubrication condition
Due to the small contact area between the flank face and the machined surface, the heat as generated in the third deformation zone is extremely small compared to the first and second deformation zones, which can be ignored. Therefore, the cutting heat generated in the third deformation zone was not analyzed in this work.

### 2.3.3 The highest temperature on tool rake face under different cutting fluids

In order to optimize the type of cutting fluid and inhibit tool wear effectively, the temperature variations under different cutting fluids were calculated by using the above established model of cutting temperature field. The cutting fluids include kerosene, absolute ethanol, castor oil, and polyethylene glycol. According to related literature [37], the thermal conductivities of these four cutting fluids are 0.13 W/m · K, 0.1531 W/m · K, 0.200 W/m · K, and 0.285 W/m · K, respectively.

Different lubricants lead to a change in the coefficient of friction between the tool-chip, which, according to the literature, is obtained as follows: 0.015, 0.017, 0.0235, 0.0278. Under the same cutting parameters, the calculated maximum temperatures on tool rake face are presented in Fig. 4.

As can be seen from Fig. 4, kerosene has the best cooling effect. This is because kerosene has a low viscosity and a small contact angle on the workpiece material, which is beneficial to the wetting of kerosene on the tool-chip contact face. As a result, the friction between the tool rake face and the chip is relieved. The reductions of friction finally decrease the cutting temperature of tool rake face. For the polyethylene glycol, however, the temperature of rake face is the highest. The reason is that the viscosity of polyethylene glycol is the largest, and the contact angle on the workpiece material is the greatest. It is difficult to spread on the tool-chip contact face. Due to the degradation in reducing the friction and promotion of heat exchange at the tool-chip interface, the highest temperature is resultantly observed on tool rake face when employing the polyethylene glycol as cutting fluid.

According to the Usui wear rate model [38], i.e., Eq. (28), the wear rate of cutting tool is proportional to the exponential power of temperature. The higher the cutting temperature is, the more intense the tool wear does, which means that reducing the temperature of tool is an effective way to suppress the wear of micro diamond tool:

\[
\frac{\partial W}{\partial t} = M \cdot V_{sb} \cdot \sigma_n \cdot \exp \left(-\frac{N}{T}\right)
\]

(28)

where \(\frac{\partial W}{\partial t}\) is tool wear rate, i.e., the wear volume of tool per unit time. \(\sigma_n\) is the contact stress in the wear zone. \(T\) is the cutting temperature. \(M\) and \(N\) are the material property-dependent constants, and \(M = 6.524 \times 10^{-11}\) m² MPa and \(N = 1483\) K. \(V_{sb}\) is the relative sliding velocity between the tool and the chip.
By using Eq. (28), the wear volume of micro diamond tool under different cutting fluids can be successfully calculated, and the results of which are presented in Fig. 5. It can be seen that the wear degree of micro diamond tool is different under different cutting fluids. Anhydrous ethanol and kerosene have the best inhibition to the wear of tool. As discussed above, the anhydrous ethanol and kerosene has a small viscosity, which are beneficial to the reduction of friction at the tool-chip interface. Resultantly, the temperature on the rake face is the lowest, and the tool wear is the lowest too.

3 Experimental validations

3.1 Preparation of micro diamond tool

In order to validate the theoretical models as developed above, a micro diamond cutting tool was prepared in a commercial available machine tool, PG3B. The rake face and flank face were both oriented with the (100) crystal plane, and a cylindrical shape was configured for the flank face. Moreover, the specific parameters of the test tool are shown in Table 1.

The cutting edge waviness and corner nose radius of the prepared micro diamond tool were evaluated by a professional instrument, i.e., the DTRC microscope system. The measuring results are shown in Fig. 6. In Fig. 6, the ideal cutting edge corresponds to the measured corner nose radius. The curve fluctuated around the ideal cutting edge is the actual profile of the cutting edge, through which the cutting edge waviness can be evaluated. The results revealed that the test micro diamond tool has a cutting edge waviness of 0.03 μm over an opening angle of 80°.

The cutting edge radius of the prepared micro diamond tool was evaluated by an atomic force microscope (AFM), i.e., the Nanite B supplied by Nanosurf Ltd. Figure 7 shows AFM scanning images of 3D topography and 2D cross-section of tool cutting edge, through which a cutting edge radius of 30.9 nm is read.

3.2 Selection of cutting parameters

Cutting experiments were carried out on a home-made ultra-precision machine tool. To validate the inhibitory effect of different cutting fluids on the wear of micro diamond tool, the spindle speed, cutting depth, and feed rate were invariable. The spindle speed was set to 1000 r/min. The cutting depth and feed rate were configured as 2 μm and 2 μm/r. Four different cutting fluids were employed. Moreover, a 6061 aluminum alloy substrate with a diameter of 100 mm was employed as the workpiece.

When finishing the whole end face of the substrate, the cutting distance of tool is calculated as

$$L = \frac{\pi r_1^2 f}{10^3}$$

where \( r_1 \) is the diameter of the workpiece. \( f \) is the feed rate. \( L \) is the cutting distance.

4 Results and discussions

In diamond turning, the machined surface roughness is an important index to evaluate the performance of diamond tool. The criterion that a diamond tool cannot be used is
that the machined surface roughness exceeds the assigned value. In general, the wear of diamond tool has a significant influence on the achieved surface roughness.

To inhibit the wear of diamond tool, many solutions had been proposed, e.g., gas shielding, ultra-low temperature cooling, ultrasonic vibration-assisted cutting, surface modification, MQL. The MQL has the best effect in inhibiting the wear of diamond tool with the satisfactory cutting efficiency and workpiece accuracy. Therefore, in this work, the MQL method was used to increase the life of micro diamond tool.

The cutting fluids can be classified into two types, cooling and lubricating. As well known, the wear mechanism of diamond tool heavily depends on the material properties of the workpiece, which leads to different inhibition effects of different cutting fluids on the wear of diamond tool. Using a suitable cutting fluid in response to the wear mechanism is of significant benefit to inhibit the wear of diamond tool.

The cutting distance related wear band width on the flank face is usually adopted to characterize the wear of diamond tool. The width of wear band can be deduced from the actual profile of the worn cutting edge acquired by the DTRC microscope system. Figures 8 and 9 present
the top view of the worn cutting edge and the polar diagram of the cutting edge waviness, respectively. It can be seen that the blue curve coupled with waviness in Fig. 9 has the similar variation tendency with the SEM observed contour of the worn cutting edge in Fig. 8. Therefore, it is possible to measure the radial wear length and the wear band length from the DTRC acquired cutting edge profile.

As shown in Fig. 9, the wear band length $l$ is first measured. The worn cutting edge (blue curve) intersects the ideal cutting edge at points A and B. As defined in Fig. 6b, the ideal cutting edge is fitted with the least square circle method, yielding the mean tool nose radius, and the worn cutting edge fluctuates around the ideal cutting edge. The wear band length can be approximated as the length of arc AB. The radial wear length $b$ is measured as the peak-valley value of the fluctuation of the worn cutting edge, i.e., the difference between the smallest tool nose radius $r_1$ and the largest tool nose radius $r_2$. By using the measured wear band length $l$ and radial wear length $b$, the wear band width can be predicted in terms of the geometries of tool tip. Finally, the wear volume can be calculated with the known width and length of the wear band. The measured results of tool cutting edge waviness at different cutting distances are shown in Fig. 10.

Based on the Usui wear rate model, i.e. Equation (28), and the measured cutting edge waviness of the worn tool shown in Fig. 10, the wear volumes of the worn tool at different cutting distances can be calculated, which are summarized in Fig. 11. It can be seen from Fig. 11 that the theoretical wear volume is always larger than the experimental wear volume. This is because the convective heat transfer of cutting fluid is not considered when modeling the temperature field on tool rake face in this work. As a result, the actual tool temperature is smaller than the predicted temperature, which in turn results in the actual wear volume being smaller than the theoretical wear volume. However, the predicted trend of tool wear volume under different cutting fluids is well consistent with the experimental one.

In order to reveal the underlying mechanism of tool wear inhibition by different cutting fluids, Raman spectroscopy and EDS analysis on the wear areas in response to dry cutting and MQL conditions were carried out. When tool cutting distance is 10 km, the results of Raman spectrum analysis are shown in Fig. 12.

In Fig. 12, it can be seen that the graphite wear takes place on diamond tool surface in dry cutting, while no graphite wear occurs under MQL condition. The experimental observations validate that the appropriate use of
cutting fluid can effectively slow down the graphitic wear of diamond tool.

Figure 13 shows the EDS analysis results of the wear zone produced under dry cutting and MQL cutting. Table 2 presents the element sorts and contents of the wear zone. The EDS analysis results acquired at different points almost have no difference, i.e., only the carbon (99.01%) and oxygen (0.99%) elements appear on the wear zone, regardless of the usage of cutting fluid. Such observations reveal that in cutting of 6061 aluminum alloy with micro diamond tool, the diffuse wear does not occur on diamond tool surface in both dry cutting and MQL cutting.

All the experimental results demonstrate that in dry cutting of 6061 aluminum alloy, the diamond tool mainly suffers from the graphitization wear and scratch wear. The factors responsible for the graphitization of diamond include the high stress and temperature. Under MQL condition, the cutting fluid can relieve the friction at the tool-chip contact surface, which in turn reduces the friction force applied to the tool surface. As a result, the stress distributed on the cutting region can be effectively reduced. On the other hand, the cutting fluid can take away some of the heat by means of thermal convection, which reduces the temperature on the rake face. Consequently, no graphite wear is observed on the micro diamond tool in MQL cutting.
This work aims to establish the temperature field model of micro diamond tool under the condition of minimum quantity lubrication and optimize the cutting fluid in inhibiting the wear of micro diamond tool. According to the theoretical modeling, related analyses, and experimental validations, some important conclusions can be drawn as follows.

1. Based on the Fourier heat conduction theory, a cutting temperature field model is firstly established to solve the maximum temperature on tool rake face under dry cutting condition. Secondly, regarding the boundary film as a layer of heat-conduction medium, the cutting temperature field model is further modified to predict the temperature on tool rake face under minimum quantity lubrication condition. The prediction results indicate that the minimum quantity lubrication method can effectively reduce the temperature on tool rake face.

**5 Conclusion**

This work aims to establish the temperature field model of micro diamond tool under the condition of minimum quantity lubrication and optimize the cutting fluid in inhibiting the wear of micro diamond tool. According to the theoretical modeling, related analyses, and experimental validations, some important conclusions can be drawn as follows.

1. Based on the Fourier heat conduction theory, a cutting temperature field model is firstly established to solve the maximum temperature on tool rake face under dry cutting condition. Secondly, regarding the boundary film as a layer of heat-conduction medium, the cutting temperature field model is further modified to predict the temperature on tool rake face under minimum quantity lubrication condition. The prediction results indicate that the minimum quantity lubrication method can effectively reduce the temperature on tool rake face.
2. The maximum temperature on tool rake face under different cutting fluids is calculated with the well-established cutting temperature field model. The results demonstrate that the lower the viscosity of the cutting fluid, the more effective the cutting fluid in reducing tool temperature. Low viscosity is beneficial to the wetting of cutting fluid on tool-chip contact face, which can relieve the friction at tool-chip interface as more as possible. The reduction of friction finally decreases the temperature on tool rake face.

3. The wear volumes of micro diamond tool are calculated in terms of the predicted cutting temperature and Usui wear rate model, and the variation trend of which agrees well with the experimental results. Such satisfactory consistency confirms that the cutting fluid can effectively reduce the cutting temperature and inhibit the wear of tool. Raman spectrum analysis further reveals that the graphite wear of micro diamond tool inevitably takes place in dry cutting, and the contribution of cutting fluid is to slow down the graphitization of diamond. The results of EDS analysis indicate that no diffusion wear occurs on the micro diamond tool in dry or minimum quantity lubrication cutting of 6061 aluminum alloy.

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Declarations

Ethics approval The authors declare that there is no ethical issue applied to this article.

Consent to participate The authors declare that all the authors have read and approved to submit this manuscript to IJAMT.

Consent for publication The authors declare that all the authors agree to sign the transfer of copyright for the publisher to publish this article upon acceptance.

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