1. Introduction

The purpose of mathematical modeling of processes and phenomena occurring in natural objects is to obtain new knowledge about these objects and processes. Certainly, the basic knowledge of Lake Baikal is knowledge of the system of currents, against which all chemical, biological, environmental and other processes develop. In the 70s of the last century, the author's work was one of the first to study the hydrodynamics of the lake using mathematical modeling methods (Tsvetova, 1977). Since then, models have occupied their niche in Baikal studies due to efforts of Russian and foreign scientists (see the review by Ovchinnikova and Bocharov, 2017).

Features of modeling natural processes are the presence of a large number of uncertainties in the formulation of models, in setting parameters. Despite the long history of studying the lake, not everything is clear in the cause-and-effect relationship, especially in interdisciplinary research. Methods of computer implementation also make their own requirements. In modern models with the necessary description of geometric scales, a large number of parameters are required. In practice, it turns out that there is always not enough data for adequate reproduction of processes.

We use a scenario approach, which in this situation is the main way to achieve results. It allows you to get a variant assessment of the results depending on the specified parameters.

2. Material and methods

To date, the author has created a complex of mathematical models of various degrees of complexity for studying processes on the large and local scales. For its implementation, algorithms, programs and modeling technology have been developed. Until recently, the basic model of the hydrodynamics was a three-dimensional non-stationary model in the non-hydrostatic approximation; its first version is presented in (Tsvetova, 1999). Since hydrodynamics is responsible for the distribution of impurities that pollute the lake, a necessary complement to the complex is a set of impurity distribution models.

With the discovery of methane hydrates at the bottom of the lake, new problem statements and, consequently, new model formulations have emerged (Tsvetova, 2015). In particular, a mathematical model of a multiphase system has been developed, which is formulated in the so-called Euler-Euler statement (Nigmatulin, 1990). In it, the phases are assumed to be interpenetrating continua. It is believed that water is the main carrier medium.

3. Results and discussion

To demonstrate the capabilities of models and scenarios, the report presents the results of calculations with various options for specifying sources of pollution associated with the development of tourism on Lake Baikal.

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Baikal. The simulation is based on a three-dimensional non-stationary non-hydrostatic model of the lake. We are talking about hypothetical scenarios for the development of lake pollution processes during one summer tourist season. To increase generality, it is not a specific year and season that is considered, but the so-called “climatic” scenarios of atmospheric influences, when data on wind fields and their operational characteristics are set in accordance with the classification from (Atlas, 1977). Using these data in the Monte Carlo method, atmospheric impact scenarios are compiled. In turn, atmospheric scenarios are taken into account in boundary conditions on the surface of the lake. Together with the calculated thermal regime of the lake, taking into account the seasonal and intraday variability of the heat balance on the surface, they are responsible for the formation of the current system. Simultaneously with the system of currents, propagation of impurities are reproduced. In this case, the impurities are considered as passive tracers. The sources of impurities in the scenarios are hypothetical tourist sites located on the shores of the lake.

Impurity propagation results are compared in various scenarios. Their analysis suggests that the functioning of tourist facilities should be regulated when assessing and planning the development of the industry in order to preserve the lake as a World Heritage Site.

4. Conclusion

In conditions of increased load on the ecosystem of the lake, which has already led to a change in the species composition of its inhabitants (Kravtsova et al., 2020), there is an urgent need for regulatory measures on the part of the competent authorities. Quantitative information, even in hypothetical scenarios such as those presented in the report, may be useful. Mathematical modeling, coupled with the scenario approach, just provides a working tool for evaluations, but it needs data to adjust to the real state of the lake system.

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