COLD GAS ACCRETION BY HIGH-VELOCITY CLOUDS AND THEIR CONNECTION TO QSO ABSORPTION-LINE SYSTEMS

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ABSTRACT

We combine H I 21 cm observations of the Milky Way, M31, and the local galaxy population with QSO absorption-line measurements to geometrically model the three-dimensional distribution of infalling neutral–gas clouds ("high-velocity clouds" (HVCs)) in the extended halos of low-redshift galaxies. We demonstrate that the observed distribution of HVCs around the Milky Way and M31 can be modeled by a radial exponential decline of the mean H I volume-filling factor in their halos. Our model suggests a characteristic radial extent of HVCs of $R_{\text{halo}} \sim 50$ kpc, a total H I mass in HVCs of $\sim 10^5 M_\odot$, and a neutral-gas accretion rate of $\sim 0.7 M_\odot \ yr^{-1}$ for M31/Milky-Way-type galaxies. Using a Holmberg-like luminosity scaling of the halo size of galaxies we estimate $R_{\text{halo}} \sim 110$ kpc for the most massive galaxies. The total absorption cross-section of HVCs at $z \approx 0$ most likely is dominated by galaxies with total H I masses between $10^9$ and $10^{10} M_\odot$. Our model indicates that the H I disks of galaxies and their surrounding HVC population can account for 30%–100% of intervening QSO absorption-line systems with log $N(H I) \geq 17.5$ at $z \approx 0$. We estimate that the neutral-gas accretion rate density of galaxies at low redshift from infalling HVCs is $\dot{M}_{\text{H}_I}/dV/dt \approx 0.022 M_\odot \ yr^{-1} \ Mpc^{-3}$, which is close to the measured star formation rate density in the local universe. HVCs thus may play an important role in the ongoing formation and evolution of galaxies.

Key words: Galaxy: halo – ISM: clouds – quasars: absorption lines

Online-only material: color figures

1. INTRODUCTION

One crucial aspect of galaxy formation and evolution concerns the continuous infall of intergalactic gas onto galaxies. While it is clear that galaxies do accrete substantial amounts of gas from intergalactic space to power star formation, the exact way of how galaxies get their gas is still a matter of debate. In the conventional sketch of galaxy formation and evolution, gas is falling into a dark matter (DM) halo and then is shock-heated to approximately the halo virial temperature (a few $10^8$ K, typically), residing in quasi-hydrostatic equilibrium with the DM potential well (Rees & Ostriker 1977). The gas then cools slowly through radiation, condenses, and settles into the center of the potential where it forms stars as part of a galaxy ("hot mode" of gas accretion). It has been argued, however, that for smaller DM potential wells the infalling gas may radiate its acquired potential energy at much lower temperatures ($< 10^{5.5}$ K, typically), so that one speaks of the "cold mode" of gas accretion (e.g., White & Rees 1978). For the cold mode of gas accretion the star formation rate of the central galaxy is directly coupled to its gas accretion rate (White & Frenk 1991). Numerical simulations indicate that for individual galaxies the dominating gas accretion mode depends on the mass and the redshift (e.g., Birnboim & Dekel 2003; Kereš et al. 2005). The general trend for $z \approx 0$ is that the hot mode of gas accretion dominates for massive galaxies with DM-halo masses $> 10^{12} M_\odot$, while the cold accretion mode dominates for galaxies with smaller DM-halo masses (e.g., van de Voort et al. 2011).

Independently of the theoretically expected gas accretion mode of galaxies it has been known for a long time that galaxies at low and high $z$ are surrounded by large amounts of neutral and ionized gas that partly originates in the intergalactic medium (IGM). This material is complemented by neutral and ionized gas that is expelled from the galaxies as part of galactic fountains, galactic winds, and from merger processes (see, e.g., Richter 2006 for a review). Because the interplay between these circumgalactic gas components is manifold and the gas physics of such a turbulent multi-phase medium is complex, the circulation of neutral and ionized gas in the inner and outer halos currently cannot be modeled in full detail in hydrodynamical simulations. To improve current models of galaxy evolution it is of imminent importance to quantify the amount of cool, neutral gas in and around galaxies from observations and search for observational strategies to separate metal-deficient infalling intergalactic gas from metal-enriched gaseous material that is circulating in the circumgalactic environment of galaxies as a result of fountain processes and galaxy mergers.

In the Milky Way and other very nearby spiral galaxies (e.g., M31), the infall of neutral gas onto the disks can be observed directly by H I 21 cm observations of extraplanar gas clouds that move through the halos of these galaxies. For the Milky Way, the so-called high-velocity clouds (HVCs) represent the prime candidates for neutral gas that is being accreted onto the Milky Way disk. HVCs represent high-latitude gaseous structures (located in the Galactic halo) observed in H I 21 cm emission at high radial velocities, $|v_{LSR}| > 100$ km s$^{-1}$ (e.g., Wakker & van Woerden 1998; Richter 2006). Halo clouds with somewhat smaller radial velocities in the range $|v_{LSR}| = 50–100$ km s$^{-1}$ are commonly referred to as "intermediate-velocity clouds" (IVCs). Throughout this paper, we will use the expression "HVC" for all neutral halo clouds (including IVCs), if not otherwise stated. The total neutral-gas mass of the Milky Way’s HVC population is on the order of $10^7 M_\odot$ and the total accretion rate of neutral gas in the form of HVCs has been estimated to be $\sim 0.5 M_\odot \ yr^{-1}$ (e.g., Wakker et al. 2007, 2008; Wakker 2004). Also, M31 exhibits a population of neutral halo clouds in a
similar mass range (for simplicity, hereafter also referred to as “HVCs”; Thilker et al. 2004). These observations, together with \( \text{H}_\text{i} \) 21 cm measurements of other nearby galaxies (e.g., Sancisi et al. 2008), imply that HVCs represent a common phenomenon in the local universe.

Another important method to study the gaseous outskirts of galaxies and their relation to the cosmic web is the analysis of intervening absorption-line systems in optical and ultraviolet (UV) spectra of QSOs (active galactic nuclei (AGNs)). QSO absorption spectroscopy allows us to detect both neutral and ionized gas in the IGM and the halos of galaxies over eight orders of magnitude in column density and over more than 90% of the age of the universe. It is therefore a particularly sensitive method to explore the multi-phase nature of circumgalactic gas and its origin (e.g., Bergeron & Boissé 1991; Steidel et al. 2002; Charlton & Churchill 1998; Ding et al. 2005; Richter et al. 2011).

In this paper, we combine \( \text{H}_\text{i} \) 21 cm observations of the HVC population of Milky Way and M31 with 21 cm data of the local galaxy population and QSO absorption-line measurements to study the three-dimensional distribution of (partly) neutral-gas structures in the extended halos of low-redshift galaxies. While several previous studies have linked the Galactic HVC population to intervening QSO absorbers based on various arguments (e.g., Blitz et al. 1999; Charlton et al. 2000; Pisano et al. 2004; Mshar et al. 2007; Schaye et al. 2007; Narayanan et al. 2008; Richter et al. 2009; Stocke et al. 2010; Ribaudo et al. 2011b), a detailed geometrical HVC model that connects key observables (column densities, covering fractions, absorber number densities) of HVCs and intervening absorbers with the gas accretion rates of galaxies at low redshift has not been presented so far. The main goal of the present study is to model the radial distribution of HVC analogs in halos as a function of galaxy mass and size, determine their absorption cross-section at \( z \approx 0 \), and estimate the neutral-gas accretion rate of galaxies at low redshift.

We refrain from including \( \text{H}_\text{i} \) 21 cm observations of HVCs from other galaxies beyond the Local Group in our study because these observations are strongly limited in sensitivity for detecting diffuse neutral halo gas (e.g., Oosterloo et al. 2007). In addition, beam-smearing effects are known to smooth out the true spatial distribution of individual halo clouds in more distant galaxies, so that the observed filling factor of \( \text{H}_\text{i} \) 21 cm in these systems does not provide a realistic estimate for the absorption cross-section of this gas.

The paper is organized as follows: in Section 2, we discuss \( \text{H}_\text{i} \) 21 cm observations of the HVC population of the Milky Way and M31. In Section 3, we develop a simple model for the radial distribution of neutral gas in the halos of these galaxies. In Section 4, we generalize our HVC model for the local galaxy population, based on information on the \( \text{H}_\text{i} \) mass function of low-redshift galaxies and the absorption cross-section of damped Ly\( \alpha \) absorbers (DLAs) and Lyman limit systems (LLS) at \( z \approx 0 \). The relation between HVCs and intervening QSO absorbers is discussed in Section 5. In Section 6, we present the conclusions from our study.

2. HIGH-VELOCITY CLOUDS IN THE HALOS OF THE MILKY WAY AND M31

2.1. HVCs in the Milky Way

The HVC population of the Milky Way has a total sky covering fraction of \( f_c \approx 0.30 \) for column densities \( N(\text{H}_\text{i}) \geq 7 \times 10^{17} \text{ cm}^{-2} \) and \( f_c \approx 0.15 \) for column densities \( N(\text{H}_\text{i}) \geq 2 \times 10^{18} \text{ cm}^{-2} \) (Wakker 2004, and references therein). The largest Milky Way HVC is Complex C, which covers \( \sim 1500 \text{ deg}^2 \) on the sky (\( f_c \approx 0.04 \)). With a low metallicity of \( \approx 0.15 \) solar (e.g., Fox et al. 2004; Richter et al. 2001) and a distance of \( D \sim 10 \text{ kpc} \) (Wakker et al. 2007; Thom et al. 2008), Complex C most likely is a cloud that is being accreted from the IGM or from a satellite galaxy. The Magellanic Stream (MS) also covers an area of \( \sim 1500 \text{ deg}^2 \), but most likely has a distance as large as \( D \sim 50 \text{ kpc} \) (Gardiner & Noguchi 1996). The MS represents a tidal feature expelled from the Magellanic Clouds as they move through the extended Milky Way halo. With its large distance and its stream-like shape the MS is clearly distinct from most of the other Galactic HVCs, which predominantly are less extended and located at distances \( < 15 \text{ kpc} \) from the disk (Wakker et al. 1999, 2007, 2008; Thom et al. 2006, 2008).

Other prominent Galactic HVCs are Complex A, Complex H, the Anti-Center Cloud, and Complexes WA–WE. Covering fractions and distances for some of these complexes (as far as known) are summarized in Table 1. Because accurate distance information on the Milky Way HVCs is still limited, the total \( \text{H}_\text{i} \) mass in HVCs and the \( \text{H}_\text{i} \) mass accretion rate are not well constrained. The currently available information implies \( M_{\text{H}_\text{i},\text{HVC}} \sim 3 \times 10^8 \text{ M}_\odot \) and \( dM_{\text{H}_\text{i},\text{HVC}}/dt \sim 0.5 \text{ M}_\odot \text{ yr}^{-1} \) (Wakker et al. 2007, 2008; Wakker 2004). The \( \text{H}_\text{i} \) column densities in HVCs follow a column-density distribution function (CDFD) in the form \( f(N_{\text{H}_\text{i}}) \propto N_{\text{H}_\text{i}}^{-\beta} \) with \( \beta = 1.42 \) for \( \log N(\text{H}_\text{i}) \geq 18 \) (Lockman et al. 2002).

2.2. The M31 HVC Population

As has been shown by Braun et al. (2009), M31 has an \( \text{H}_\text{i} \) disk that extends to radii of \( r \approx 30 \text{ kpc} \) for column densities above \( \log N(\text{H}_\text{i}) \geq 20.3 \). Beyond \( r \approx 30 \text{ kpc} \) the \( \text{H}_\text{i} \) disk appears to be truncated (Braun et al. 2009; Braun & Thilker 2004). The HVC population of M31 was studied in detail with the Green Bank Telescope (GBT) by Thilker et al. (2004). These authors detected more than 20 individual HVCs around M31 with \( \text{H}_\text{i} \) column densities \( \geq 5 \times 10^{17} \text{ cm}^{-2} \) and estimated a total \( \text{H}_\text{i} \) mass of the HVCs of \( 3-4 \times 10^7 \text{ M}_\odot \) (see also Thilker et al. 2005).

In the left panel of Figure 1 we show the distribution of HVCs around the M31 disk, based on the GBT \( \text{H}_\text{i} \) 21 cm contour map presented by Thilker et al. (2004). The HVC population of M31 reaches out until \( \sim 50 \text{ kpc} \) with a strongly decreasing HVC covering fraction toward larger radii. We assume \( D = 785 \pm 25 \text{ kpc} \) as distance for M31 (McConnachie et al. 2005), so that absolute distance estimates derived from

| HVC Name | \( f_{\text{HVC}} \) | \( D \) (kpc) |
|----------|----------------|-------------|
| Complex A | 0.01 | 8–10 |
| Complex C | 0.04 | ~10 |
| Complex H | 0.01 | >5 |
| Magellanic stream | 0.04 | ~50 |
| Complexes WA, WB | 0.01 | 8–20 |

Notes:

References: Wakker (2001, 2004); Wakker et al. (1999, 2007); B. P. Wakker (2011, private communication); Thom et al. (2006, 2008); Gardiner & Noguchi (1996).

b Sky-covering fraction of HVC gas.

c Distance.
angular coordinates are uncertain by \(\sim 3\%\). Some interesting conclusions about the radial distribution of neutral gas around M31 can be drawn from this HVC distribution map. Figure 1, right panel, shows the radius-dependent projected covering fraction \(f_{\text{HVC}}(r)\), of the HVC population of M31 plotted against \(r\) (indicated by the filled boxes), where \(r\) is the projected radius. To calculate \(f_{\text{HVC}}(r)\) we have resampled the M31 HVC map of Thilker et al. (2004) and have transformed the \((\alpha, \delta)\) coordinate system into a polar coordinate system with coordinates \(r\) and \(\theta\) centered on M31. For each ring with radius \(r\) and thickness \(r \pm \Delta r\) the parameter \(f_{\text{HVC}}(r)\) then was derived by comparing the area covered by HVC gas with the total ring area. The error bars for \(f_{\text{HVC}}(r)\) shown in Figure 1 have been calculated assuming Poisson-like statistics. Starting from \(f_{\text{HVC}} \approx 0.5\) at \(r = 15\) kpc the covering fraction decreases to values less than 0.05 for radii larger than \(r = 45\) kpc. This trend for \(f_{\text{HVC}}(r)\) can be fitted by an exponential of the form \(f_{\text{HVC}}(r) = x \exp(-r/y)\) with \(x = 2.1 \pm 0.2\) and \(y = 12.0^{+0.7}_{-0.5}\), as shown by the solid red line in the right panel of Figure 1. An exponential fit to the extraplanar H\(^{\text{I}}\) features of M31 was also favored by Braun & Thilker (2004), who analyzed lower-resolution 21 cm data of M31 from the Westerbork Synthesis Radio Telescope (WSRT).

For the inner regions of the M31 halo at \(r < 15\) kpc no HVC data are available. As discussed by Thilker et al. (2004), this does not imply that this region is devoid of HVC material. The lack of data for the disk–halo interface region at \(r < 15\) kpc (Figure 1, left panel), rather, indicates the incompleteness of the HVC map for small radii because of the confusion of neutral halo gas with the H\(^{\text{I}}\) disk of M31 together with the stringent selection criteria defined by Thilker et al. to unambiguously identify HVC features. In the Milky Way, the disk–halo interface at \(r < 15\) kpc is filled with large amounts of neutral gas that gives rise to 21 cm emission at intermediate and high velocities (e.g., Wakker 2004). Nearby edge-on galaxies such as NGC 891 also exhibit large amounts of neutral gas in the disk–halo interface region extending several kpc above and below the disk (see Sancisi et al. 2008). 21 cm measurements of NGC 891 show that the (projected) covering fraction of neutral gas is \(f_{\text{H1}} = 1\) for vertical distances \(d < 10\) kpc to the midplane of the NGC 891 disk (Oosterloo et al. 2007). If we extrapolate \(f_{\text{HVC}}\) for M31 to small radii using the exponential defined above, \(f_{\text{HVC}}\) becomes unity for \(r \leq 9\) kpc, in line with the extraplanar gas distribution observed in NGC 891. If we define \(r_3\) as the radius beyond which the projected covering fraction of HVCs falls below 3%, we derive for M31 a value of \(r_3 = 50 \pm 6\) kpc. The 1\(\sigma\) error reflects the uncertainties in the exponential parameters for \(f_{\text{HVC}}(r)\).

As shown by Braun & Thilker (2004), the high-resolution 21 cm H\(^{\text{I}}\) data of M31 from Thilker et al. (2004) follow a “standard” H\(^{\text{I}}\) CDDF of the form \(f(N_{\text{H1}}) \propto N_{\text{H1}}^{-\beta}\) with \(\beta = 1.5\) in the column-density range \(\log N(\text{H}\text{I}) = 18\)–20. The slope is very similar to the one derived for the Milky Way HVCs (Lockman et al. 2002; Section 2.1) and is in good agreement with values derived for low-redshift QSO H\(^{\text{I}}\) absorption-line systems (see Section 5.1).

3. GEOMETRICAL MODELING OF HVCs IN THE LOCAL GROUP

3.1. Modeling Setup

To combine the observational information on the HVC population of the Milky Way and M31 we have developed the custom-written numerical code Halecapd, which is based on a simple geometrical model assuming spherical symmetry. The code allows us to model the radial distribution of gas in the halos of galaxies, its mass distribution, and its absorption cross-section from any given vantage point inside and outside the sphere. Because of the unknown size distribution of HVCs we here do not attempt to model individual H\(^{\text{I}}\) clouds as HVC analogs, but instead consider the volume-filling factor of neutral gas as main input parameter, from which all relevant physical quantities (e.g., projected covering fraction, H\(^{\text{I}}\) column density, and H\(^{\text{I}}\) mass) can be easily obtained and compared to observations.

To support the model with the necessary observational data, we assume that the HVC populations of the Milky Way and M31 are identical in a statistical sense (same radial distribution and same volume-filling factor of gas with log \(N(\text{H}\text{I}) \geq 17.5\)). In view of the similarity of both galaxies in terms of morphology, mass, luminosity, etc., this assumption is justified. As mentioned above, the key parameter that describes the spatial distribution of HVCs in our spherical model is the radius-dependent volume-filling factor of optically thick HVC gas with log \(N(\text{H}\text{I}) \geq 17.5\), \(f_{\text{H1}}(r)\), where \(R\) is the physical radius (compared to the...
projected radius $r$). Because the projected (area) covering fraction of HVCs in the M31 halo can be described by an exponential (see above), we assume that $f_{v, \text{HVC}}(R)$ follows an exponential too, so that we write

$$f_{v, \text{HVC}} = f_{v, 0} \exp \left( -R/h_{\text{HVC}} \right).$$

In this equation, $f_{v, 0}$ is the volume-filling factor in the center of the sphere and $h_{\text{HVC}}$ is the scale height of the HVC population. Another important parameter in our model is the mean H I volume density $\langle n_{\text{H I}} \rangle$ in the HVC gas, as $\langle n_{\text{H I}} \rangle$ together with $f_{v, \text{HVC}}(R)$ determines the neutral-gas mass in HVCs per radial bin (= radial volume element), $M_{\text{H I}}(r) = f_{v, \text{HVC}}(R) \langle n_{\text{H I}} \rangle \mu m_{\text{H I}}$, with $m_{\text{H I}}$ as hydrogen mass and $\mu$ as a factor that corrects for the presence of helium and heavy elements in the gas. In addition, $\langle n_{\text{H I}} \rangle$ determines the mean H I column density, $\langle N(\text{H I}) \rangle$, measured along any line of sight through the halo, since $\langle N(\text{H I}) \rangle = \langle n_{\text{H I}} \rangle d$, where $d$ is the absorption path length through the halo. The parameters $\langle N(\text{H I}) \rangle$ and $\langle n_{\text{H I}} \rangle$ are constrained by 21 cm observations and ionization models of Galactic IVCs and HVCs. Note that in this study we do not model the gas physics in the halo clouds, but consider only the spatial distribution of neutral halo gas, its H I column-density distribution, its total mass, and its infall rate.

To model the sky covering fraction of neutral gas from a vantage point inside the sphere (i.e., to model the projected neutral-gas distribution in the Milky Way halo from the position of the Sun) we introduce additional constraints based on results from 21 cm observations of IVCs and HVCs. First, we only consider H I gas as neutral halo gas if it is located at vertical distances $z > 600$ pc from the midplane of the disk (whose orientation can be chosen in the model). Second, we separate neutral halo gas close to the disk (small $z$-heights) from more distant halo clouds via the parameter $z_{\text{HVC}}$. This parameter enables us to distinguish between IVCs ($z \leq z_{\text{HVC}}$) and HVCs ($z > z_{\text{HVC}}$). Finally, the parameter $v_{\text{infall}}$ defines the infall velocity of the neutral halo gas; $v_{\text{infall}}$ can be a function of $R$ or $z$, or can be chosen to be constant for IVCs and HVCs, respectively. The neutral-gas (mass) accretion rate per radial bin then is given by $dM_{\text{H I}}(r)/dt = M_{\text{H I}}(r) v_{\text{infall}}/r$.

### 3.2. Modeling Results

Using our geometrical model we are able to reproduce the observed properties of the HVC population of the Milky Way and M31 using appropriate values for the above discussed input parameters. Our favorite model is summarized in Table 2. In this model, the scale height of the HVC population is $h_{\text{HVC}} = 6.67^{+0.53}_{-0.41}$ kpc and the central volume-filling factor of neutral halo gas is $f_{v, 0} = 0.0185 \pm 0.0036$. The errors have been determined numerically; they reflect the 1σ error range of the exponential parameters for $f_{v, \text{HVC}}$ in M31 (Section 2.2). In our model we assume that IVCs and HVCs are separated at a $z$-height of $z_{\text{HVC}} = 5$ kpc, in line with what is known about the distribution of IVC and HVC distances in the Milky Way halo (Wakker et al. 2007, 2008; Thom et al. 2006, 2008).

Only these three parameters ($h_{\text{HVC}}, f_{v, 0},$ and $z_{\text{HVC}} = 5$) are required to reproduce the observed exponential decline of the projected covering fraction of the HVC population of M31 ($f_{v, \text{HVC}} = 2.1 \exp(-r/12)$ for radii $r \geq 9$ kpc) from a vantage point outside the sphere and the observed covering fractions of $\sim 30\%$ for IVCs and HVCs from a vantage point inside the sphere (see Section 2). Note that for $r < 9$ kpc the projected covering fraction is set to unity. The characteristic radial extent of the HVC population around both galaxies is $r_{3} = 50 \pm 6$ kpc. The mean projected covering fraction of neutral IVC/HVC gas in the halo region is $f_{v, \text{HVC}} = 0.21 \pm 0.02$.

Observations of H I, metal ions, and molecular hydrogen suggest that the neutral hydrogen volume densities in IVCs and HVCs may span a large range over at least three orders of magnitude ($10^{-2} \leq n_{\text{H I}} \leq 10$ cm$^{-3}$; e.g., Wakker et al. 1999; Wakker 2004; Richter et al. 2003a, 2003b, 2009; Sembach et al. 2001). For our model we adopt a value of $n_{\text{H I}} = 0.1$ cm$^{-3}$, which is close to the one that has been derived for high-velocity cloud Complex C (Wakker et al. 1999). We consider this value as a realistic estimate for the volume-averaged mean neutral hydrogen density in IVCs and HVCs. As infall velocity we adopt $v_{\text{infall}} = 100$ km s$^{-1}$ for IVCs and 50 km s$^{-1}$ for HVCs, assuming that the (vertical) infall velocities toward the disk are comparable to the observed radial velocities of IVCs and HVCs. Since the infall velocity of HVCs is determined by the balance between the gravitational force and the ram-pressure force provided by
the surrounding hot coronal gas (e.g., Benjamin & Danly 1997; Brüns & Mebold 2004), a more precise modeling of $v_{\text{infall}}$ would also require the modeling of the density distribution of hot halo gas, which is beyond the scope of this study. However, from grid-based hydrodynamical simulations of HVCs Heitsch & Putman (2009) derive infall velocities that are very similar to the velocities adopted by us.

With the above given values for $n_{H_1}$ and $v_{\text{infall}}$ the mean H I column density in IVCs and HVCs (from the interior view) is $\langle N(H_1) \rangle = 1.3 \times 10^{19} \text{ cm}^{-2}$, the total H I mass in the halo at $r < r_3$ is $M_{H_1,\text{halo}} = 1.2 \times 10^8 M_\odot$, and the total H I mass accretion rate for gas at $r < r_3$ is $dM_{H_1,\text{halo}}/dt = 0.74 M_\odot \text{ yr}^{-1}$. These values are in excellent agreement with the observations (see Section 2).

4. MODELING OF GALAXY ABSORBERS

4.1. Galaxies and Their Absorption Characteristics

In Section 3, we have demonstrated that it is possible to reproduce the statistical properties of the HVC population of the Milky Way and M31 using a model that is based on very simple geometrical assumptions. In the following, we want to generalize our HVC model for the local galaxy population to constrain the absorption cross-section of HVCs in the local universe.

Galaxies and their circumgalactic gaseous environment can be traced by intervening absorption lines of H I and metal ions in the spectra of distant QSOs and AGNs. The strongest intervening neutral-gas absorbers are the so-called DLAs, which have H I column densities $\log N(H_1) \geq 20.3$. These systems contain a substantial fraction of the neutral-gas mass in the universe (Wolfe et al. 1995). Although there is still no consistent picture about the host galaxies of DLAs, observations suggest that a mixed population of galaxies contributes to the absorption cross-section of DLAs at $z \approx 0$ (e.g., Turnshek et al. 2001; Chen & Lanzetta 2003; Rao et al. 2003). From H I 21 cm observations of the local galaxy population Zwaan et al. (2005) conclude, however, that the total DLA cross section at $z \approx 0$ is dominated by the gaseous disks of L* and sub-L* galaxies with H I masses $> 10^9 M_\odot$.

Based on H I 21 cm observations of the Milky Way, M31, and other nearby galaxies it is expected that neutral-gas absorbers in the extended halos of galaxies (i.e., HVC analogs) have H I column densities below that of DLAs (e.g., Wakker 2004; Thilker et al. 2004; Lockman et al. 2002; Murphy et al. 1995). Using the common absorber classification scheme, halo absorbers therefore are expected to be seen as the so-called sub-DLAs (19.0 $\leq \log N(H_1) < 20.3$) and LLS (17.2 $\leq \log N(H_1) < 19.0$). A large fraction of the LLS at low redshift therefore may represent distant analogs of the HVCs seen around the Milky Way and M31 (Richter et al. 2011).

As for HVCs, the H I column-density distribution function of intervening QSO absorbers at low and high redshifts below the DLA column-density limit can be fitted by a power law in the form $f(N_{H_1}) \propto N_{H_1}^{-\beta}$. For QSO absorbers, $\beta$ has values between 1 and 2, depending on redshift and the column-density interval chosen (see Lehner et al. 2007). Unfortunately, $\beta$ is poorly constrained for $\log N(H_1) > 16$ at $z = 0$ due to the limited amount of low-redshift H I absorption-line data in the UV. In contrast, for high $z$ there exists a large database that allows us to constrain $\beta$ at a relatively high accuracy (Ribaudo et al. 2011a).

The incidence of intervening DLAs, sub-DLAs, and LLS in QSO spectra, usually expressed by the quantity $dN_{\text{LLS}}/dz$, the number of optically thick H I absorbers per unit redshift, can be obtained from the integration of the H I CDDF over the appropriate column-density range (in our case $\log N(H_1) > 17.5$). Moreover, $dN_{\text{LLS}}/dz$ is proportional to the space density of galaxies, $n_{\text{gal}}$, and the mean geometrical cross section of optically thick H I, $\langle A_{H_1} \rangle$, in these galaxies:

$$\frac{dN_{\text{LLS}}}{dz} = \int_{N_{H_1,\text{LLS}}} \frac{f(N_{H_1}) dN_{H_1}}{\langle A_{H_1} \rangle} = \frac{c n_{\text{gal}} \langle A_{H_1} \rangle}{H(z)}. \quad (2)$$

We adopt $H(z) = H_0 (\Omega_m (1 + z)^3 + \Omega_\Lambda)^{1/2}, H_0 = 73 \text{ km s}^{-1} \text{ Mpc}^{-1}, \Omega_m = 0.238,$ and $\Omega_\Lambda = 0.762$ (Spergel et al. 2007). We assume that the covering fraction of optically thick H I gas is $f_{\text{HVC}} = 1$ in the (inclined) disk of a galaxy and $f_{\text{HVC}} < 1$ in the surrounding halo, where H I arises in the form of HVCs. Let $A_{\text{disk}}$ be the geometrical cross section of the (inclined) disk and $A_{\text{halo}} = \pi R_{\text{halo}}^2$ the cross section of the (spherical) halo region with radius $R_{\text{halo}}$. We then can introduce an effective HVC cross section for an individual galaxy, $A_{\text{HVC,eff}} = (f_{\text{HVC}}) (A_{\text{halo}} - A_{\text{disk}})$, so that the total area covered by optically thick H I in and around a galaxy is $A_{H_1} = A_{\text{disk}} + A_{\text{HVC,eff}}$.

From H I 21 cm measurements of the local galaxy population, Zwaan et al. (2005) have derived a DLA number density per unit redshift of $(dN/dz)_{\text{DLA}} = 0.045 \pm 0.006$, a result that is in good agreement with previous estimates (e.g., Rosenberg & Schneider 2003; $(dN/dz)_{\text{DLA}} = 0.053 \pm 0.013$). These measurements provide direct information on the individual geometrical cross section (i.e., $A_{\text{disk}}$) of the gaseous disks at $\log N(H_1) > 20.3$ in low-redshift galaxies for a large range of galaxy morphologies and luminosities. These H I surveys are, however, not sensitive enough and do not provide sufficient spatial resolution to identify a possibly existing HVC population in the halos of these galaxies.

Based on the above-given relations, a QSO sightline passing through both an H I disk and H I gas of a galaxy would show a DLA as an absorption signature, while a sightline passing only through an optically thick HVC would exhibit a sub-MLA or LLS. We then can write for the total number density of H I absorbers with $\log N(H_1) > 17.5$ that trace gas disks of galaxies and their surrounding HVC population:

$$\frac{dN}{dz}_{\text{disk+HVC}} = \left( \frac{dN}{dz} \right)_{\text{DLA}} + A_{\text{disk}}/A_{\text{disk}} + A_{\text{HVC,eff}}. \quad (3)$$

Our goal is to estimate $A_{\text{HVC,eff}}$ from a generalized version of our HVC model for the local galaxy population (for which $A_{\text{disk}}$ is known). This will enable us to estimate $(dN/dz)_{\text{disk+HVC}}$ and link the HVC population at $z = 0$ with the H I column-density distribution function of low-redshift QSO absorbers.

4.2. On the Absorption Cross-section of Neutral-gas Disks

Before we start to investigate the absorption cross-section of neutral gas in the halos of galaxies, it is useful to briefly discuss the relation between the absorption cross-section, the total H I mass, and the scale length of neutral-gas disks in local galaxies, as derived from H I 21 cm surveys. Using 21 cm data from Arecibo and the Very Large Array (VLA) Rosenberg & Schneider (2003) have studied in detail these and other properties of 50 nearby galaxies in the context of the low-redshift DLA population. Rosenberg & Schneider find
that the total (inclination-corrected) H\textsubscript{i} cross section of gas disks in their galaxy sample in the DLA column-density range (log \(N_H > 20.3\)) is given by \(A_{\text{disk}} = \pi ab/4\), where \(a\) and \(b\) are the major and minor axis parameters (in kiloparsecs) derived at the DLA column-density limit (see also Rosenberg \& Schneider 2003, their appendix). They also find a remarkably tight correlation between \(A_{\text{disk}}\) and the total H\textsubscript{i} mass of the disk, \(M_{\text{HI}}\) (in solar mass units), as \(\log A_{\text{disk}} = \log M_{\text{HI}} - 6.82\).

Since the mean value for \(b\) in a sample of randomly inclined gas disks is expected to be 0.637\(a\), we can write for the mean disk area \(A_{\text{disk}} \approx 0.16 \pi a^2 = 0.5a^2\) or log \(A_{\text{disk}} \approx 2 \log a - 0.3\). Combining this with the observed relation between \(A_{\text{disk}}\) and \(M_{\text{HI}}\), we obtain a relation between the total H\textsubscript{i} mass and the disk radius at the DLA limit in the form \(\log a = 0.5 \log M_{\text{HI}} - 3.26\). Finally, Rosenberg \& Schneider (2003) find a (weak) correlation between the H\textsubscript{i} mass and the J-band luminosity in their sample, \(\log M_{\text{HI}} = 0.44 \log L_J + 5.27\), where \(L_J\) is in solar luminosity units.

4.3. On the Absorption Cross-section of HVCs Surrounding Neutral-gas Disks

Surveys of the local galaxy population, such as the one presented by Rosenberg \& Schneider (2003), show that galaxies span several orders of magnitude in parameters like H\textsubscript{i} mass, optical luminosity, and H\textsubscript{i} disk size. One crucial question that concerns the cross section of neutral gas in the halos of these galaxies is how the size of the gaseous halo of a galaxy is related to the above-listed parameters.

The standard approach to scale the size of a galaxy’s gaseous halo with its luminosity is to adopt a Holmberg-like luminosity scaling, so that the halo radius is given by

\[ R_{\text{halo}}(L) = R_\star \left( \frac{L}{L_\star} \right)^{\delta}, \tag{4} \]

where \(\delta \approx 0.2\) and \(R_\star \approx 110\) kpc for B-band luminosities, as derived from analyses of intervening Mg\textsubscript{II} absorbers (which trace neutral and ionized gas in disks and halos) and their relation to galaxies (Steidel 1995; Kacprzak et al. 2008). It can be shown that with the above-given relations between \(L_J\), \(M_{\text{HI}}\), and \(A_{\text{disk}}\) a Holmberg-like luminosity scaling as given by Equation (4) corresponds to a linear scaling of the halo radius with the H\textsubscript{i} disk radius. This is because \(M_{\text{HI}} \propto L_{\text{J}}^{0.44}\) (Rosenberg \& Schneider 2003) and \(a \propto M_{\text{HI}}^{1/2}\), which leads to \(R_{\text{halo}} \propto L_{\text{J}}^{0.22} \propto \alpha\), i.e., a Holmberg-like luminosity scaling with \(\delta = 0.22\). For the following, we therefore assume a Holmberg-like luminosity scaling with \(\delta = 0.22\), but we parameterize the halo size over the relation \(R_{\text{halo}}(a) = \gamma a\), where \(\gamma > 1\) and \(a\) is the H\textsubscript{i} disk radius for H\textsubscript{i} column densities above the DLA limit. For M31 \(\gamma \approx 1.7\) (see Section 2.2).

To characterize the covering fraction of HVCs, \(f_{\text{HVC}}\), in galaxy halos, we assume that the exponential decline of \(f_{\text{HVC}}\) observed in M31 reflects a general behavior of HVCs in galaxies in the local universe. We then can express the projected covering fraction of HVCs around galaxies as a function of its H\textsubscript{i} disk length in the form

\[ f_{\text{HVC}}(r) \approx \begin{cases} 1 & : \ r \leq 0.3 \ a \\ 2.1 \cdot \exp (-2.5 \ r/a) & : \ r > 0.3 \ a \end{cases}. \tag{5} \]

For M31, \(a = 30\) kpc (Braun et al. 2009; see above). In Figure 2, left panel, we show \(f_{\text{HVC}}(r)\) for four different H\textsubscript{i} masses. Analogous to what has been discussed for the M31 HVC population, we define \(r_3\) as the halo radius, beyond which \(f_{\text{HVC}}\) falls below the 3\% level and set \(R_{\text{halo}} = r_3\). The scaling relation between the disk and halo radius in our model then comes out to \(R_{\text{halo}} = 1.69 a\) for all halo radii considered (i.e., \(\gamma = 1.69\)).

Since \(\log a = 0.5 \log M_{\text{HI}} - 3.26\) (see above), Equation (5) allows us to calculate the sizes of neutral-gas halos of low-redshift galaxies as a function of their H\textsubscript{i} mass and luminosity. It also enables us to predict the cross section and number density of sub-DLAs and LLS that represent HVC analogs, their radial distribution, and estimate the neutral-gas accretion rate of galaxies in the local universe.

4.4. Modeling Results

As the input for our generalized HVC model we adopt the H\textsubscript{i} mass distribution of low-redshift DLAs from
Zwaan et al. (2005), as derived from a high-resolution 21 cm survey of the local galaxy population. Using 21 cm data from the WRST Zwaan et al. (2005) have studied the H\textsc{i} properties of 355 nearby galaxies and their contribution to the local DLA population. The expected values of $(dN/dz)_\mathrm{DLA}$ for the different H\textsc{i} masses of the galaxies in their sample are shown as gray shaded area in the right panel of Figure 2. Obviously, galaxies with H\textsc{i} masses in the range log $M_{\text{H\textsc{i}}}$ = 8.8–10.0 dominate the absorption cross-section of DLAs at $z = 0$.

Based on these data, we derive for each galaxy H\textsc{i} mass bin the radius and area of the H\textsc{i} disk and the H\textsc{i} halo using the above-discussed relations. Note that here we do not take into account the possibility that the neutral-gas disks of galaxies significantly extend below the DLA column-density limit. Using our generalized HVC model we then calculate for each mass bin the radius-dependent (projected) HVC covering fraction $(f_{HVC})$, the effective HVC cross section $(A_{\text{HVC}})$, and the expected number density of disk/halo H\textsc{i} absorbers (Equation (3)). Moreover, our model calculates for each galaxy H\textsc{i} mass bin the mean projected HVC covering fraction $(f_{HVC})$, the total neutral-gas mass in HVCs $(M_{\text{H\textsc{i},HVC}})$, and the neutral-gas mass accretion rate $(dM_{\text{H\textsc{i}}}/dt)$. For the infall velocities we adopt the values for $v_{\text{infall}}$ for IVCS and HVCs listed in Table 2. The expected number densities $(dN/dz)_{\text{disk/HVC}}$ as a function of the galaxy H\textsc{i} mass are indicated with the gray shaded area in the right panel of Figure 2. All results are summarized in Table 3. Based on these results we derive the following relation between the H\textsc{i} disk mass of galaxies, log $M_{\text{H\textsc{i}}}$ (in solar units), and the radius of the neutral-gas halo, $R_{\text{halo}}$ (in (kpc)):

$$\log R_{\text{halo}} = 0.5 \log M_{\text{H\textsc{i}}} - 3.03. \quad (6)$$

If we integrate the values of $(dN/dz)_{\text{disk/HVC}}$ listed in Table 3 over the entire mass range, we derive a total number density of disk/halo absorbers of $(dN/dz)_{\text{disk/HVC}} = 0.212$. This value is $\sim$5 times larger than the number density of DLAs at $z = 0$ (Zwaan et al. 2005), suggesting that the absorption cross-section of HVCs with log $N(HI) >= 17.5$ exceeds that of DLAs by a factor of $\sim$4, on average. As for DLAs, the total absorption cross-section of optically thick H\textsc{i} in disks and halos is dominated by galaxies in the mass range log $M_{\text{H\textsc{i}}} = 8.8–10.0$.

As our model indicates, the mean (projected) covering fraction of HVCs in galaxy halos is small, $(f_{HVC}) = 0.2$, typically.

### 4.5. Neutral-gas Accretion Rate Density

Using the mass accretion rates $(dM_{\text{H\textsc{i}}}/dt)$ listed in Table 3 together with the H\textsc{i} mass function of the local galaxy population (Zwaan et al. 2005) we can estimate the neutral-gas accretion rate density of HVCs (mass accretion rate per unit volume) at low redshift. We obtain $dM_{\text{H\textsc{i}}}/dt/dV = 0.022 M_\odot \text{yr}^{-1} \text{Mpc}^{-3}$. Note that this value is calculated under the assumption that all of the neutral gas in the halos of galaxies is being accreted onto their disks, independently of its origin inside or outside the host galaxies. The above estimate does not include the mass of the ionized gas component of HVCs, which may contribute substantially to the total mass of multi-phase halo clouds (e.g., Fox et al. 2010; Winkel et al. 2011). Also not included are partly neutral-gas fragments with masses and angular sizes below the detection limit of 21 cm HVC surveys. Such structures are known to exist in the Milky Way halo (Richter et al. 2009), but their (total) neutral-gas mass most likely is small compared to the large, extended 21 cm HVCs. The role of ionized gas is further discussed below.

The value of $0.022 M_\odot \text{yr}^{-1} \text{Mpc}^{-3}$ is remarkably close to the star formation rate density at $z = 0$ ($\rho_\star = 0.01$–0.02 $M_\odot \text{yr}^{-1} \text{Mpc}^{-3}$), as derived from ultraviolet and infrared observational data (Hopkins & Beacom 2006). Therefore, cold-gas accretion by HVCs possibly plays an important (if not dominating) role in feeding galaxies at $z \approx 0$ with gaseous material to power star formation.

The above-given value for the accretion rate density can also be compared with recent estimates of the "cold-mode" gas accretion rate densities at $z = 0$ from cosmological simulations. Using a smoothed particle hydrodynamics (SPH) code, Kereš et al. (2009) find $dM/dt/dV \sim 0.03 M_\odot \text{yr}^{-1} \text{Mpc}^{-3}$ for cold gas that never exceeded a maximum temperature of $T_{\text{max}} = 2.5 \times 10^5$ K. However, using SPH simulations with more realistic gas physics, van de Voort et al. (2011) derive a much lower "cold-mode" gas accretion rate density for galaxies at $z = 0$ of $dM/dt/dV \sim 0.002 M_\odot \text{yr}^{-1} \text{Mpc}^{-3}$, while for the superordinate DM halos the cold-mode accretion rate is estimated to be $dM/dt/dV \sim 0.01 M_\odot \text{yr}^{-1} \text{Mpc}^{-3}$, thus five

### Table 3

Properties of H\textsc{i} Absorbing Galaxies

| $\log M_{\text{H\textsc{i},disk}}$ ($M_\odot$ in Mpc$^{-2}$) | $\log A_{\text{disk}}$ (A in kpc$^2$) | $r_s$ (kpc) | $(f_{HVC})$ | $\log A_{\text{HVC},eff}$ (A in kpc$^2$) | $(dN/dz)_{\text{disk/HVC}}$ | $\log M_{\text{H\textsc{i},HVC}}$ ($M_\odot$ in Mpc$^{-2}$) | $dM_{\text{H\textsc{i}}}/dt$ ($M_\odot$ in Mpc$^{-2}$) |
|-----------------|------------------|-------|----------|-----------------|-----------------|-----------------|-----------------|
| 6.7–7.0         | 0.03             | 2     | 0.35     | 0.41            | $7.1 \times 10^{-4}$ | 3.38            | $5.9 \times 10^{-5}$ |
| 7.0–7.3         | 0.33             | 3     | 0.23     | 0.88            | $1.9 \times 10^{-3}$ | 4.21            | $3.7 \times 10^{-4}$ |
| 7.3–7.6         | 0.63             | 4     | 0.21     | 0.97            | $8.4 \times 10^{-4}$ | 4.82            | $1.4 \times 10^{-3}$ |
| 7.6–7.9         | 0.93             | 7     | 0.15     | 1.51            | $5.9 \times 10^{-4}$ | 5.46            | $5.2 \times 10^{-3}$ |
| 7.9–8.2         | 1.23             | 9     | 0.17     | 1.73            | $6.1 \times 10^{-3}$ | 5.91            | $1.2 \times 10^{-2}$ |
| 8.2–8.5         | 1.53             | 13    | 0.18     | 2.05            | $1.3 \times 10^{-2}$ | 6.39            | $3.1 \times 10^{-2}$ |
| 8.5–8.8         | 1.83             | 19    | 0.18     | 2.40            | $1.7 \times 10^{-2}$ | 6.85            | $7.5 \times 10^{-2}$ |
| 8.8–9.1         | 2.13             | 27    | 0.19     | 3.00            | $3.8 \times 10^{-2}$ | 7.73            | 0.40            |
| 9.1–9.4         | 2.43             | 39    | 0.19     | 3.30            | $3.9 \times 10^{-2}$ | 8.15            | 0.85            |
| 9.4–9.7         | 2.73             | 55    | 0.20     | 3.61            | $3.8 \times 10^{-2}$ | 8.56            | 1.69            |
| 9.7–10.0        | 3.03             | 78    | 0.20     | 3.91            | $1.8 \times 10^{-2}$ | 8.95            | 3.09            |
| 10.0–10.3       | 3.33             | 90    | 0.22     | 3.91            | $1.8 \times 10^{-2}$ | 8.95            | 3.09            |

Notes: $^a$ Explanations: $r_s$, halo radius beyond which the projected HVC covering fraction is $\lesssim 3\%$; $A_{\text{disk}}$, H\textsc{i} disk area; $(f_{HVC})$, mean projected HVC covering fraction for halo region; $A_{\text{HVC,eff}} = A_{\text{HVC}}(A_{\text{halo}} - A_{\text{disk}})$; $(dN/dz)_{\text{disk/HVC}}$, number density of disk/halo absorbers with log $N(HI) >= 17.5$ (per galaxy H\textsc{i} mass bin); $M_{\text{H\textsc{i},HVC}}$, total neutral-gas mass in HVCs per galaxy; $dM_{\text{H\textsc{i}}}/dt$, neutral-gas mass infall rate per galaxy.
times higher. Therefore, only 20% of the cold gas that enters the DM halo in their simulation is actually being accreted as cold gas by the central galaxy. Unfortunately, these studies do not provide information on the absorption cross-section of all the cold gas in the DM halos and its radial distribution around the galaxies (independently of whether it is being accreted or not), so that a detailed comparison between the simulation results and our HVC model is not possible at this point.

It needs to be mentioned that gas that is considered “cold” in the cosmological simulations does not necessarily end up as H\textsc{i} high-velocity gas that is detectable via 21 cm observations. It is expected that a substantial fraction of the accreted gas that never was heated up to the virial temperature of the host halo remains diffuse and “warm,” i.e., at low densities (\(n_{\text{HI}} < 10^{-2} \text{ cm}^{-3}\)) and intermediate temperatures (\(T = 10^2–10^5 \text{ K}\)). The neutral-gas fraction in such warm gas is expected to be low, so that it remains unseen in H\textsc{i} 21 cm emission (“warm” mode of gas accretion; Heitsch & Putman 2009; Bland-Hawthorn 2009). The existence of such a warm, ionized gas component in the halos of galaxies is strongly supported by the detection of intermediate- and high-ion absorption (e.g., from Si\textsc{iii}, C\textsc{iii}, C\textsc{iv}, and Si\textsc{iv}) in the halo of the Milky Way (e.g., Fox et al. 2006; Sembach et al. 1995, 1999) and in the circumgalactic environments of other galaxies (e.g., Ribaudo et al. 2011b). Also, the ionized envelopes of 21 cm HVC complexes represent significant gas reservoirs that need to be considered for a realistic estimate of the total (neutral and ionized) gas mass that is being accreted by galaxies (e.g., Winkel et al. 2011; Fox et al. 2010). The contribution of the ionized gas component to the total gas infall rate is difficult to determine; however, the infall velocity of ionized gas may be substantially lower than for neutral gas because of hydrodynamical effects that affect the ionized cloud envelopes, such as gas stripping, turbulent mixing, and heat conduction. The same processes also affect the total cloud mass and the neutral-gas fraction in HVCs and thus influence the H\textsc{i} volume-filling factor in these clouds. These aspects clearly are best resolved through high-resolution hydrodynamical simulations (e.g., Heitsch & Putman 2009; Vieser & Hensler 2007).

5. HVCs AND THEIR RELATION TO INTERVENING QSO ABSORBERS

5.1. HVCs and H\textsc{i} Ly\textalpha Absorbers

To estimate the contribution of H\textsc{i} HVCs to the number density of optically thick H\textsc{i} Ly\textalpha absorbers at low \(z\), it is necessary to know the H\textsc{i} CDDF for log \(N(\text{H}\textsc{i}) > 17.5\) at low redshift (Equation (2)). As mentioned above, the CDDF at \(z = 0\) is poorly constrained for this column-density range owing to the fact that high column-density H\textsc{i} absorbers are rare and that the amount of the QSO absorption-line data in the ultraviolet is limited. Corbelli & Bandiera (2002) have combined absorption-line data for intermediate redshifts from Bandiera & Corbelli (2001), low-redshift absorption data from Weymann et al. (1998), and 21 cm H\textsc{i} emission-line data from Ryan-Weber et al. (2003) to construct the H\textsc{i} CDDF in the range \(N(\text{H}\textsc{i}) = 13–21\). The CDDF presented in Corbelli & Bandiera (2002) can be fitted by power laws in the ranges log \(N(\text{H}\textsc{i}) > 18\) and log \(N(\text{H}\textsc{i}) > 20\), while at log \(N(\text{H}\textsc{i}) = 18–20\) there seems to be a plateau in \(f(N(\text{H}\textsc{i}))\). Since this is exactly the column-density range of relevance for HVCs, these data imply that the total absorption cross-section of HVCs increases only mildly with a decreasing H\textsc{i} cutoff column density. To check the validity of this interesting feature in \(f(N(\text{H}\textsc{i}))\) more absorption-line data for the range log \(N(\text{H}\textsc{i}) > 18–20\) are required. To compare the frequency of sub-DLAs and LLS at low redshift with the HVC absorption cross-section obtained from our model, we have combined the absorption/emission-line data from Corbelli & Bandiera (2002) and Zwaan et al. (2005) and have constructed a “hybrid” H\textsc{i} CDDF at \(z \approx 0\), in Figure 3, left panel, shown as the solid line.

Independent constraints for \(f(N(\text{H}\textsc{i}))\) at low redshift come from the study by Lehner et al. (2007), who have analyzed low-redshift Ly\textalpha absorbers based on high-resolution HST/STIS data. While their study is limited to the column-density range log \(N(\text{H}\textsc{i}) = 13–16.5\), it is possible to extrapolate their CDDF from the three data points between log \(N(\text{H}\textsc{i}) = 14.5–16.5\) (Lehner et al. 2007; their Figure 14) and log \(N(\text{H}\textsc{i}) = 20\) with a

\[
\frac{dN}{dz} \approx \frac{N(\text{H}\textsc{i})}{10^{21} \text{ cm}^{-2}}.
\]
power law $f(N) \propto N^{-\beta}$, where $\beta \approx 1.3$ (Figure 3, left panel, dashed line). This extrapolation nicely connects to the 21 cm data from Zwaan et al. (2005), but lies substantially above the H I CDDF based on the Corbelli et al. results. For the following, we consider both representations of the H I CDDF shown in Figure 3 as plausible input parameters to estimate the absorption cross-section of H I in sub-DLAs and LLS at $z \approx 0$. In a recent study, Ribaudo et al. (2011a) have compiled a large sample of LLS, most of them located at high redshifts ($z \lesssim 2.6$). Interestingly, their data points for $f(N)$ fit well to the H I CDDF extrapolated from the Lehner et al. (2007) data.

Figure 3, right panel, shows the (cumulative) number density of H I absorbers per unit redshift, $(dN/dz)_{-N(H I)}$, as a function of the cutoff H I column density, N(H I), derived from integrating the two representations of the H I CDDF over all column densities larger than N(H I) (Equation (2)). This plot now can be directly compared to the results from our HVC model. The gray shaded area indicates the allowed $dN/dz$ range (90–100% contribution of HVCs to the H I absorber population) for the hybrid H I CDF (Corbelli & Bandiera 2002; Zwaan et al. 2005; left panel, solid line), while the gray shaded plus green shaded area shows the allowed $dN/dz$ range based on the H I CDDF extrapolated from the Lehner et al. (2007) data (left panel, dashed line). The red filled circle indicates the value for $(dN/dz)_{\text{disk+HVC}}$ derived from our HVC model. Thus, our HVC model predicts a value for $dN/dz$ from H I disk and halo absorbers that lies slightly above the value expected from the hybrid CDF, but lies at a ~30% level of $dN/dz$ predicted by the CDDF extrapolated from the Lehner et al. (2007) data. We conclude that HVCs in our model contribute with 30–100% to the population of H I Ly$\alpha$ absorbers with log N(H I) $\gtrsim$ 17.5 at $z \approx 0$. Most likely, the contribution of HVCs is clearly less than 100%, as extended neutral and partly ionized gas disks with log N(H I) $\lesssim$ 20.3 and galaxy outflows (as traced by strong Mg II absorption; see Section 5.2) contribute to the population of Ly$\alpha$ absorbers in the LLS and sub-DLA column-density range.

A more detailed comparison between the absorption cross-section of HVCs and the local H I Ly$\alpha$ absorber population has to await a more precise determination of the H I CDDF at $z \approx 0$ from HST/COS data.

5.2. HVCs and Intervening Mg II Absorbers

The Mg II resonant doublet near 2800 Å is commonly used to study neutral and ionized gas in the outskirts of galaxies at $0.3 < z < 2.2$ (e.g., Bergeron & Boissé 1991; Charlton & Churchill 1998; Ding et al. 2005). The so-called strong Mg II systems represent intervening metal absorbers in QSO spectra that have rest-frame equivalent widths $W > 0.3$ Å in the Mg II $\lambda$2796 line. They are commonly found within 35kpc of luminous galaxies and thus most likely are related to neutral and ionized gas in the disks and halos of low-redshift galaxies. The number density of strong intervening Mg II systems in the local universe is expected to be $(dN/dz)_{\text{MgII}} \approx 0.5$, as estimated from extrapolating the redshift evolution of strong Mg II systems in the Sloan Digital Sky Survey data from $z > 0.3$ down to $z \approx 0$ (Nestor et al. 2005).

The value for $(dN/dz)_{\text{MgII}}$ is $2-3$ times higher than $(dN/dz)_{\text{disk+HVC}}$ estimated from our HVC model, suggesting a substantially larger absorption cross-section of strong Mg II systems compared to HVC H I absorbers with log N(H I) $\gtrsim$ 17.5. This is expected, because with an ionization potential of $15$ eV Mg II traces both neutral and ionized gas in the disks and halos of galaxies. Kacprzak et al. (2008) estimated an Mg II covering fraction of $(f_{\text{MgII}}) \approx 0.5$ for galaxies and their gaseous halos from a sample of 37 Mg II selected galaxies at intermediate redshift. This is roughly two times the mean value for $(f_{\text{disk+HVC}})$ in our HVC model.

In the Milky Way halo, the Mg II absorption cross section in HVCs has not been determined yet, mostly because of the lack of appropriate high-resolution near-UV data. The covering fractions of other low and intermediate ions with strong transitions in the far-UV (FUV) and with ionization potentials comparable to that of Mg II (e.g., C II, Si II) are larger than the covering fraction of optically thick H I (Richter et al. 2009), but not large enough to explain the high value for $(dN/dz)_{\text{MgII}}$ in the local universe. Recent studies suggest, indeed, that many strong Mg II absorbers at low redshift arise in bipolar outflows and galactic winds (e.g., Bond et al. 2001; Bouché et al. 2011) and thus are related to halo environments with larger Mg II covering fractions in galaxies that are more actively star forming than the Milky Way and M31. From our estimate for $(dN/dz)_{\text{disk+HVC}}$ we conclude that the contribution of infalling gas clouds (HVCs) to the absorption cross section of strong Mg II absorbers most likely is small, but not negligible ($<35\%$).

5.3. HVCs and Intervening Ca II Absorbers

Next to the Mg II doublet in the near-UV, the two Ca II H&K lines in the optical near 4000 Å represent valuable tracers for neutral gas in the inner and outer regions of galaxies. For instance, Ca II absorption is frequently observed in Galactic HVCs (e.g., Richter et al. 2005; Ben Bekhti et al. 2008) and is used as diagnostic line to derive distance brackets for IVCs and HVCs from optical data (e.g., Wakker et al. 2007, 2008; Thom et al. 2006, 2008). Based on archival high-resolution optical spectra of more than 300 QSOs obtained with the VLT/UVES spectrograph Richter et al. (2011) have investigated intervening Ca II absorbers at $z \approx 0.5$ and their relation to disk and halo gas components. They derive a number density per unit redshift of $(dN/dz)_{\text{CaII}} = 0.117 \pm 0.044$ for Ca II systems with log N(Ca II) $\gtrsim$ 11.65, which is roughly 55% of the cross section of H I HVCs with log N(H I) $\gtrsim$ 17.5 estimated from our model.

In the Milky Way halo, the covering fraction of Ca II for log N(Ca II) $\gtrsim$ 11.65 is $\approx$0.2 (Ben Bekhti et al. 2008), thus ~67% of that 21 cm HVCs with log N(H I) $\gtrsim$ 17.5. As discussed in Richter et al. (2011), Ca II absorbers with log N(Ca II) $\gtrsim$ 11.65 predominantly trace neutral-gas clouds with log N(H I) $\gtrsim$ 18.5. This is due to the presence of dust in the gas (Ca is strongly depleted into dust grains) and the mostly sub-solar metallicities of the absorbers. From these numbers it follows that intervening Ca II absorbers arise only in specific regions in HVCs, where the H I column density is large enough to compensate for the Ca dust-depletion and abundance effects.

6. CONCLUSIONS

Several previous studies have discussed a possible link between intervening metal-line and H I absorbers in QSO spectra and the HVC phenomenon in the Milky Way (e.g., Blitz et al. 1999; Charlton et al. 2000; Mshar et al. 2007; Narayanan et al. 2008; Richter et al. 2009; Stocke et al. 2010; Ribaudo et al. 2011b). In this study, we move this idea forward by bringing together in a quantitative manner the properties of HVCs in the Milky Way and M31, QSO absorption-line statistics, and neutral gas accretion rates of galaxies in the local universe. We demonstrate that it is possible to explain the star formation rate
density in the local universe through the infall of cold gas in the form of HVCs by using a simple geometrical model. In this model we project the observed statistical properties of the H I HVCs in the Local Group onto the local galaxy population, assuming a Holmberg-like luminosity scaling of the halo size. The main results from our modeling are summarized in Tables 2 and 3.

We emphasize at this point that we have not tuned any of the input parameters to fit the HVC cross section to the H I absorber population or any other above-discussed QSO absorber observables. Our generalized HVC model is based solely on observed properties of the HVC population in the Local Group and the local galaxy population without any further assumptions. Note that the exact radial dependence of projected HVC covering fraction, $f_{HVC}(r)$ (here assumed to be an exponential, based on the M31 data), is unimportant for the total absorption cross section of HVCs, as only the effective area $A_{HVC, eff}$ (i.e., the product of total halo area and the mean HVC covering fraction) is relevant for $(dN/dz)_{HVC}$ in a sample of randomly distributed QSO sightlines. However, because the shape of $f_{HVC}(r)$ reflects the volume-filling factor and thus the mass distribution of neutral gas around galaxies, $f_{HVC}(r)$ is closely related to the H I accretion rate of galaxies $dM_{H I}(r)/dt = M_{H I}(r) v_{\text{infall}}/r$. Thus, for a more precise estimate of the neutral-gas accretion rate of galaxies at $z = 0$ it will be important to constrain the radial distribution of HVCs around other low-redshift galaxies beyond the Local Group using sensitive, high-resolution 21 cm observations. Such observations need to be accompanied by a more precise estimate of the dynamics of neutral-gas structures along their infall path through the hot coronal gas in the halos of galaxies of different masses, e.g., from hydrodynamical simulations (Kaufmann et al. 2009; Keres & Hernquist 2009).

Since most of the gaseous material that is being accreted by galaxies at $z = 0$ may be diffuse, ionized gas (“warm accretion”; Bland-Hawthorn 2009) rather than cold, neutral gas in the form of 21 cm HVCs, it will be important for future studies to investigate the distribution and mass of ionized gas in galaxy halos. Diffuse ionized gas structures in the extended halos of galaxies are expected to have temperatures $T < 3 \times 10^4$ K, relatively low gas densities, and low neutral-gas fractions (i.e., they remain unseen in 21 cm HVC surveys). Such structures can be observed best in absorption in the FUV in the lines of low and intermediate ions such as C II, C III, Si II, and Si III (Fox et al. 2006; Ribaudo et al. 2011b). Over the next few years large amounts of such spectral data hopefully will become available from the many ongoing observational campaigns with HST/COS. Results from these observations can be easily implemented in our halo model to predict the ionized gas accretion rate for low-redshift galaxies.

In conclusion, the increasing amount of information on the distribution and physical properties of gas in the inner and outer halos of galaxies from observations, simulations, and semi-analytic models now can be used to substantially improve our understanding of gas-accretion processes of galaxies in the local universe. Our study has shown one possible way of how to combine information from the local HVC population and QSO absorption-line systems at $z = 0$ to investigate these processes for the local galaxy population. More detailed studies of this kind (e.g., including constraints on ionized halo gas) thus could be of great importance to constrain the role of gas-accretion processes for the ongoing formation and evolution of galaxies at low $z$ and to characterize their connection to the cosmic web.

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