A Generative Model of Words and Relationships from Multiple Sources

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Abstract

Neural language models are a powerful tool to embed words into semantic vector spaces. However, learning such models generally relies on the availability of abundant and diverse training examples. In highly specialised domains this requirement may not be met due to difficulties in obtaining a large corpus, or the limited range of expression in average use. Such domains may encode prior knowledge about entities in a knowledge base or ontology. We propose a generative model which integrates evidence from diverse data sources, enabling the sharing of semantic information. We achieve this by generalising the concept of co-occurrence from distributional semantics to include other relationships between entities or words, which we model as affine transformations on the embedding space. We demonstrate the effectiveness of this approach by outperforming recent models on a link prediction task and demonstrating its ability to profit from partially or fully unobserved data training labels. We further demonstrate the usefulness of learning from different data sources with overlapping vocabularies.

Introduction\textsuperscript{1}

A deep problem in natural language processing is to model the semantic relatedness of words, drawing on evidence from text and spoken language, as well as knowledge graphs such as ontologies. A successful modelling approach is to obtain an embedding of words into a metric space such that semantic relatedness is reflected by closeness in this space. One paradigm for obtaining this embedding is the neural language model (Bengio et al. 2003), which traditionally draws on local co-occurrence statistics from sequences of words (sentences) to obtain an encoding of words as vectors in a space whose geometry respects linguistic and semantic features. The core concept behind this procedure is the distributional hypothesis of language; see Sahlgren (2008), that semantics can be inferred by examining the context of a word. This relies on the availability of a large corpus of diverse sentences, such that a word’s typical context can be accurately estimated.

In the age of web-scale data, there is abundant training data available for such models in the case of generic language. For specialised language domains this may not be true. For example, medical text data (Liu et al. 2015) often contains protected health information, necessitating access restrictions and potentially limiting corpus size to that obtainable from a single institution, resulting in a corpus with less than tens of millions of sentences, not billions as in (for example) Google n-grams. In addition to this, specialised domains expect certain prior knowledge from the reader. A doctor may never mention that aromatase inhibitor (a type of cancer drug), for example, because they communicate sparsely, assuming the reader shares their training in this terminology. In such cases, it is likely that even larger quantities of data are required, but the sensitive nature of such data makes this difficult to attain.

Fortunately, such specialised disciplines often create expressive ontologies, in the form of annotated relationships between terms (denoted by underlines). These may be semantic, such as dog is a type of animal, or derived from domain-specific knowledge, such as anemia is an associated disease of leukemia. (This is a relationship found in the medical ontology system UMLS; see Bodenreider, 2004). We observe that these relationships can be thought of as additional contexts from which co-occurrence statistics can be drawn; the set of diseases associated with leukemia arguably share a common context, even if they may not co-occur in a sentence (see Figure 1).

We would like to use this structured information to improve the quality of learned embeddings, to use their information content to regularize the embedding space in cases of low data abundance while obtaining an explicit representation of these relationships in a vector space. We tackle this by assuming that each relationship is an operator which transforms words in a relationship-specific way. Intuitively, the action of these operators is to distort the shape of the space, effectively allowing words to have multiple representations without requiring a full set of parameters for each possible sense.

The intended effect on the underlying (untransformed) embedding is twofold: to encourage a solution which is more sensitive to the domain than would be achieved using only unstructured information and to use heterogeneous sources of information to compensate for sparsity of data. In addition

\textsuperscript{1}A preliminary version of this work appeared at the International Workshop on Embeddings and Semantics at SEPLN 2015 (Hyland, Karaletsos, and Rättsch 2015).

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imatinib is a tyrosine-kinase inhibitor used in the treatment of chronic myelogenous leukemia.

architecture to predict the next word in a sequence, using distributed representations to overcome the curse of dimensionality. Since then, much work has been devoted to obtaining, understanding, and applying these distributed language representations. One such model is word2vec of Mikolov et al. (2013), which more explicitly relies on the distributional hypothesis of semantics by attempting to predict the surrounding context of a word, either as a set of neighbouring words (the skip-gram model) or as an average of its environment (continuous bag of words). We note later in the model section that the idealised version of skip-gram word2vec is a special case of our model with one relationship; appears in a sentence with. In practice, word2vec uses a distinct objective function, replacing the full softmax with an approximation intended to avoid computing a normalising factor. We retain a probabilistic interpretation by approximating gradients of the partition function, allowing us to follow the true model gradient while maintaining tractability. Furthermore, learning a joint distribution facilitates imputation and generation of data, dealing with missing data and making predictions using the model itself. We note that a generative approach to language was also explored by Andreas and Ghahramani (2013), but does not concern relationships.

Relational data can also be used to learn distributed representations of entities in knowledge graphs, entities which may correspond to or can be mapped to words. A general approach is to implicitly embed the graph structure through vertex embeddings and rules (or transformations) for traversing it. Bordes et al. (2011) scored the similarity of entities under a given relationship by their distance after transformation using pairs of relationship-specific matrices. Socher et al. (2013) describe a neural network architecture with a more complex scoring function, noting that the previous method does not allow for interactions between entities. The TransE model of Bordes et al. (2013) (and extensions such as Wang et al. (2014b), Fan et al. (2014), and Lin et al. (2015)) represents relationships as translations, motivated by the tree representation of hierarchical relationships, and observations that linear composition of entities appears to preserve semantic meaning (Mikolov et al. 2013). These approaches are uniquely concerned with relational data however, and do not consider distributional semantics from free text. Faruqui et al. (2015) and Johansson and Nieto Piña (2015) describe methods to modify pre-existing word embeddings to align them with evidence derived from a knowledge base, although their models do not learn representations de novo.

Similar in spirit to our work is Weston et al. (2013), where entities belonging to a structured database are identified in unstructured (free) text in order to obtain embeddings useful for relation prediction. However, they learn separate scoring functions for each data source. This approach is also employed by Fried and Duh (2014), Xu et al. (2014), Yu and Dredze (2014), and Wang et al. (2014a). In these cases, separate objectives are used to incorporate different data sources, combining (in the case of Xu et al. (2014)) the skip-gram objective from Mikolov et al. (2013) and the TransE objective of Bordes et al. (2013). Our method uses a single...
energy function over the joint space of word pairs with relationships, combining the ‘distributional objective’ with that of relational data by considering free-text co-occurrences as another type of relationship.

We have mentioned several approaches to integrating graphs into embedding procedures. While these graphs have been derived from knowledge bases or ontologies, other forms of graphs have also been exploited in related efforts, for example using constituency trees to obtain sentence-level embeddings (Tai, Socher, and Manning 2015).

The motivation for our work is similar in spirit to multitask and transfer learning (for instance, Caruana (1997), Evgeniou and Pontil (2004), or Widmer and Rätsch (2012)). In transfer learning one takes advantage of data related to a similar, typically supervised, learning task with the aim of improving the accuracy of a specific learning task. In our case, we have the unsupervised learning task of embedding words and relationships into a vector space and would like to use data from another task to improve the learned embeddings, here word co-occurrence relationships. This may be understood as a case of unsupervised transfer learning, which we tackle using a principled generative model.

Finally, we note that a recent extension of word2vec to full sentences (Jernite, Rush, and Sontag 2015) using a fast generative model exceeds the scope of our model in terms of sentence modeling, but does not explicitly model latent relationships or tackle transfer learning from heterogeneous data sources.

**Probabilistic Modelling of Words and Relationships**

We consider a probability distribution over triplets $(S, R, T)$ where $S$ is the source word of the (possibly directional) relationship $R$ and $T$ is the target word. Note that while we refer to ‘words’, $S$ and $T$ could represent any entity between which a relationship may hold without altering our mathematical formulation, and so could refer to multiple-word entities (such as UMLS Concept Unique Identifiers) or even non-lexical objects. Without loss of generality, we proceed to refer to them as words. Following Mikolov et al. (2013), we learn two representations for each word: $c_s$ represents word $s$ when it appears as a source, and $v_t$ for word $t$ appearing as a target. Relationships act by altering $c_s$ through their action on the vector space $(c_s \rightarrow G_R c_s)$. By allowing $G_R$ to be an arbitrary affine transformation, we combine the bilinear form of Socher et al. (2013) with translation operators of Bordes et al. (2013).

The joint model is given by a Boltzmann probability density function,

$$ P(S, R, T|\Theta) = \frac{1}{Z(\Theta)} e^{-E(S, R, T|\Theta)} $$

$$ = \frac{1}{\sum_{S,R,T} e^{-E(S, R, T|\Theta)}} $$

(1)

Here, the partition function is the normalisation factor over the joint posterior space captured by the model parameters $Z(\Theta) = \sum_{S,R,T} e^{-E(S, R, T|\Theta)}$. The parameters $\Theta$ in this case are the representations of all words (both as sources and targets) and relationship matrices; $\Theta = \{c_i, G_r, v_j\}_{i,j \in \text{vocabulary}}$. If we choose an energy function

$$ E(S, R, T|\Theta) = -v_T \cdot G_R c_S $$

(2)

we observe that the $|R| = 1$, $G_R = I$ case recovers the original softmax objective described in Mikolov et al. (2013), so the idealised word2vec model is a special case of our model.

This energy function is problematic however, as it can be trivially minimised by making the norms of all vectors tend to infinity. While the partition function provides a global regularizer, we find that it is not sufficient to avoid norm growth during training. We therefore use as our energy function the negative cosine similarity, which does not suffer this weakness:

$$ E(S, R, T|\Theta) = -\frac{v_T \cdot G_R c_S}{|v_T||G_R c_S|} $$

(3)

This is also a natural choice, as cosine similarity is the standard method for evaluating word vector similarities. Energy minimisation is therefore equal to finding an embedding in which the angle between related entities is minimised in an appropriately transformed relational space. It would be simple to define a more complex energy function (using perhaps splines) by choosing a different functional representation for $R$, but we focus in this work on the affine case.

**Inference and Learning** We estimate our parameters $\Theta$ from data using stochastic maximum likelihood on the joint probability distribution. The maximum likelihood estimator is:

$$ \Theta^* = \text{argmax} \ P(D|\Theta) = \text{argmax} \ \prod_n P((S, R, T)_n|\Theta) $$

(4)

Considering the log-likelihood at a single training example $(S, R, T)$ and taking the derivative with respect to parameters, we obtain:

$$ \frac{\partial \log P(S, R, T|\Theta)}{\partial \Theta_i} = \frac{\partial}{\partial \Theta_i} \left[ -E(S, R, T|\Theta) \right] $$

$$ - \frac{\partial}{\partial \Theta_i} \left[ \log \sum_{s,r,t} e^{-E(S, R, T|\Theta)} \right] $$

(5)

We also considered an alternate, more symmetric energy function using the Frobenius norm of $G$:

$$ E(S, R, T|\Theta) = -\frac{v_T \cdot G_R c_S}{|v_T||G_R c_S|} $$

(3)

However, we found no clear empirical advantage to this choice.
Given a smooth energy function the first term is easily obtained, but the second term is problematic. This term, derived from the partition function \( Z(\Theta) \), is intractable to evaluate in practice owing to its double sum over the size of the vocabulary (potentially \( \mathcal{O}(10^5) \)). In order to circumvent this intractability we resort to techniques used to train Restricted Boltzmann Machines and use stochastic maximum likelihood, also known as persistent contrastive divergence (PCD) (Tieleman 2008). In contrastive divergence, the gradient of the partition function is estimated using samples drawn from the model distribution seeded at the current training example (Hinton 2002). However, many rounds of sampling may be required to obtain good samples. PCD retains a persistent Markov chain of model samples across gradient evaluations, assuming that the underlying distribution changes slowly enough to allow the Markov chain chain to mix. We use Gibbs sampling by iteratively using the conditional distributions of all variables \( (S, R, T) \), see below) to obtain model samples.

In particular, we draw \( S, R \) and \( T \) from the conditional probability distributions:

\[
P(S|r, t; \Theta) = \frac{e^{-E(s, r, t)}(s, r, t; \Theta)}{\sum_s e^{-E(s, r, t)}(s, r, t; \Theta)}
\]

\[
P(R|s, t; \Theta) = \frac{e^{-E(s, r, t)}(s, r, t; \Theta)}{\sum_r e^{-E(s, r, t)}(s, r, t; \Theta)}
\]

\[
P(T|s, r; \Theta) = \frac{e^{-E(s, r, t)}(s, r, t; \Theta)}{\sum_t e^{-E(s, r, t)}(s, r, t; \Theta)}
\]

(6)

Thereby, we can estimate the gradient of \( Z(\Theta) \) at the cost of these evaluations, which are linear in the size of the vocabulary.

Using this, following the objective from (5) further simplifies to a contrastive objective given a batch of \( B \) data samples and \( M \) model samples (each model sample obtained from an independent, persistent Markov chain):

\[
\frac{\partial P(D; \Theta)}{\partial \Theta_i} \approx \frac{1}{M} \sum_{m=1}^{M} \left[ \frac{\partial E((S, R, T)_m; \Theta)}{\partial \Theta_i} \right] - \frac{1}{B} \sum_{b=1}^{B} \left[ \frac{\partial E((S, R, T)_b; \Theta)}{\partial \Theta_i} \right]
\]

(7)

Interestingly, the model can gracefully deal with missing elements in observed triplets (for instance missing observed relationships). Learning is achieved by considering the partially observed triple as a superposition of all possible completions of that triple, each weighted by its conditional probability given the observed elements, using (6). This produces a gradient which is a weighted sum.

In the fully-observed case (which we sometimes call supervised in an abuse of terminology), the weighting is simply a spike on the observed state. Similarly, the model can predict missing values as a simple inference step. These properties make having a joint distribution very attractive in practical use, offsetting the conceptual difficulty of training. In our experiments, we exploit these properties to do principled semi-supervised and unsupervised learning with partially observed or unobserved relationships without needing an external noise distribution or further assumptions.

**Implementation** We provide the algorithm in Python (https://github.com/corcra/bf2). Since most of its runtime takes place in vector operations, we are developing a GPU-optimised version. We use Adam (Kingma and Ba 2015) to adapt learning rates and improve numerical stability. We used the recommended hyperparameters from this paper: \( \lambda = 1 - 10^{-6}, \epsilon = 1 - 10^{-8}, \beta_1 = 0.9, \beta_2 = 0.999 \). Unless otherwise stated, hyperparameters specific to our model were: dimension \( d = 100 \), batch size of \( B = 100 \), learning rate for all parameter types of \( \alpha = 0.001 \), and three rounds of Gibbs sampling to obtain model samples.

**Experiments** We will proceed to explore the model in five settings. First, an entity vector embedding problem on WordNet which consists of fully observed triplets of words and relationships. In the second case we demonstrate the power of the semi-supervised extension of the algorithm on the same task. We then show that a) adding relationship data can lead to better embeddings and b) that adding unstructured text can lead to better relationship predictions. Finally, we demonstrate that the algorithm can also identify latent relationships that lead to better word embeddings.

**Data** As structured data, we use the WordNet dataset described by Socher et al. (2013), available at http://stanford.io/2EYOYH. This contains 38,588 words and 11 types of relationships. Training data consists of true triples such as (feeling, has instance, pride).

We derived an additional version of this dataset by stripping sense IDs from the words, which reduced the vocabulary to 33,330 words. We note that this procedure likely makes prediction on this data more difficult, as every word receives only one representation. We did this in order to produce an aligned vocabulary with our unstructured data source, taken to be English Wikipedia (https://dumps.wikimedia.org/, August 2014). We extracted text using WikiExtractor (http://bit.ly/11Mz1WJ). We greedily identified WordNet 2-grams in the Wikipedia text. Two words were considered in a sentence context if they appeared within a five word window. Only pairs for which both words appeared in the WordNet vocabulary were included. We drew from a pool of 112,581 training triples in WordNet with 11 relationships, and 8,206,304 triples from Wikipedia (heavily sub-sampled, see experiments). To check that our choice to strip sense IDs was valid, we also created a version of the Wikipedia dataset where each word was tagged with its most common sense from the WordNet training corpus.

We found that this did not significantly impact our results, so we chose to continue with the sense-stripped version, preferring to collapse some WordNet identities over assigning possibly-incorrect senses to words in Wikipedia.

**WordNet Prediction Task** We used our model to solve the basic prediction task described in Socher et al. (2013). In
this case, the model must differentiate true and false triples, where false triples are obtained by corrupting the \( T \) entry in the triple, e.g. \((S, R, T) \rightarrow (S, R, \tilde{T})\) (where \((S, R, \tilde{T})\) doesn’t appear in the training data). The ‘truth’ of a triple is evaluated by its energy \( E(S, R, T) \), with a relationship-specific cut-off chosen by maximizing accuracy on a validation set (this is an equivalent procedure to the task as initially described). By learning explicit representations of each of the 38,588 entities in WordNet, our approach most closely follows the ‘Entity Vector’ task in Socher et al. This is to be contrasted with the ‘Word Vector’ task, where a representation is learned for each word, and entity representations are obtained by averaging their word vectors. We elected not to perform this task because we are not confident that composition into phrases through averaging is well-justified.

Using the validation set to select an early stopping point at 66 epochs, we obtain a test set accuracy of 78.2% with an AUROC of 85.6%. The ‘Neural Tensor Model’ (NTN) described in Socher et al. (2013) achieves an accuracy of around 70% on this task, although we note that the simpler Bilinear model also described in Socher et al. (2013) achieves 74% and is closer to the energy function we employ. The improved performance exhibited by this simpler Bilinear model was also noted by Yang et al. (2015). Other baselines reported by Socher et al. were a single layer model without an interaction term, a Hadamard model (Bordes et al. 2012) and the model of Bordes et al. (2011) which learns separate left and right relationship operators for each element of the triple. These were outperformed by the Bilinear and NTN models, see Figure 4 in Socher et al. (2013) for further details. Hence, our model outperforms the two previous methods by more than 4%.

As a preliminary test of our model, we also considered the FreeBase task described by Socher et al. (2013). Initial testing yielded an accuracy of 85.7%, which is comparable to the result of their best-performing model (NTN) of about 87%. We chose not to further explore this dataset however, because its entities are mostly proper nouns and thus seemed unlikely to benefit from additional semantic data.

**Semi-supervised Learning for WordNet** We next tested the semi-supervised learning capabilities of our algorithm (see Inference and Learning). For this we consider the same task as before, but omit some label information in the training set and instead use posterior probabilities during the inference. For this we trained our algorithm with a subset of the training data (total 112,581 examples) and measured the accuracy of classifying into true and false relationships as before. The fully-observed case used only a subset of fully-observed data (varying amounts as indicated on the x-axis). For semi-supervised learning, we also used the remaining data, but masking the type of the relationship between pairs. In Figure 2 we report the accuracy for different labelled/unlabelled fractions of otherwise the same dataset. We find that the semi-supervised method consistently performs better than the fully observed method for all analysed training set sizes. In this and the previous experiment, one Markov chain was used for PCD and a \( l_2 \) regulariser on \( G_R \) parameters with weight 0.01.

**Adding Unstructured Data to a Relationship Prediction Task** To test how unstructured text data may improve a prediction task when *structured* data is scarce, we augmented a subsampled set of triples from WordNet with 10,000 examples from Wikipedia and varied the weight \( \kappa \) associated with their gradients during learning. The task is then to predict whether or not a given triple \((S, R, T)\) is a true example from WordNet, as described previously. Figure 3 shows accuracy on this task as \( \kappa \) and the amount of structured data vary. To find the improvement associated with unstructured data, we compared accuracy at \( \kappa = 0 \) with \( \kappa = \kappa^* \) (where \( \kappa^* \) gave the highest accuracy on the validation set; marked with *). We find that including free text data quite consistently improves the classification accuracy, particularly when structured data is scarce.

In this experiment and all following, we used five Markov chains for PCD and a \( l_2 \) regulariser on all parameters with weight 0.001.

**Relationship Data for Improved Embeddings** In this case, we assume *unstructured text data* is restricted, and vary the quantity of structured data. To evaluate the *untransformed* embeddings, we use them as the inputs to a supervised multi-class classifier. The task for a given \((S, R, T)\) triple is to predict \( R \) given the vector formed by concatenating \( c_S \) and \( v_T \). We use a random forest classifier trained on
Figure 3: Unstructured data helps relationship learning: In addition to training on a set of known relationships, we use unstructured data from Wikipedia with varying weight \((x\text{-axis})\) during training. As before, the goal is to predict if a triple \((S,R,T)\) is true by using its energy as a score. A validation set is used to determine the threshold below which a triple is considered ‘true’. The solid line denotes the average of three independent experimental runs; shaded areas show the range of results. The bar plot on the right shows the difference in accuracy between \(\kappa = 0\) and \(\kappa = \kappa^*\), where \(\kappa^*\) gave the highest accuracy on a validation set. Significance at 5% (paired t-test) is marked by asterisk. We find then that unstructured Wikipedia can improve relationship learning in cases when labelled relationship data is scarce.

To avoid testing on the training data (since the embeddings are obtained using the WordNet training set), we perform this procedure once for each relationship (11 times - excluding appears in sentence with), each time removing from the training data all triples containing that relationship. Figure 4 shows the F1 score of the multi-class classifier on the left-out relationship for different combinations of data set sizes. We see that for most relationships, including more unstructured data improves the embeddings (measured by performance on this task). We also trained word2vec (Mikolov et al. 2013) on a much larger Wikipedia-only dataset (4,145,372 sentences) and trained a classifier on its vectors; results are shown as black lines. We see that our approach yields a consistently higher F1 score, suggesting that even data about unrelated relationships provides information to produce vectors that are semantically richer overall.

These results illustrate that embeddings learned from limited free text data can be improved by additional, unrelated relationship data.

Unsupervised Learning Of Relationships In our final experiment, we explore the ability of the model to learn embeddings from co-occurrence data alone, without specifying the relationships it should use. When using the model with just one relationship (trivially the identity), the model effectively reverts to word2vec. However, if we add a budget of relationships (in our experiments we use 1, 3, 5, 7, 11), the model has additional parameters available to learn affine transformations of the space which can differentiate how distances and meaning interact for the word embeddings without fixing this \textit{a priori}. Our intuition is that we want to test whether textual context alone has substructure that we can capture with latent variables. We generate a training set of one million word co-occurrences from Wikipedia (using a window size of 5 and restricting to words appearing in the WordNet dataset, as described earlier), and train different models for each number of latent relationships. Inspired by earlier experiments testing the utility of supplanting WordNet training data with Wikipedia examples, we decide to test the ability of a model purely trained on Wikipedia to learn word and relationship representations which are predictive of WordNet triplets, \textit{without} having seen any data from WordNet. As a baseline we start with \(|R| = 1\) to test how well word embeddings from context alone can perform, indicated by the leftmost bar in Figure 5. We then proceed to train models with more latent relationships. We observe that, especially for some relationship prediction tasks, including this flexibility in the model produces a noticeable increase in F1 score on this task. Since we evaluate the embeddings alone, this effect must be due to a shift in the content of these vectors, and cannot be explained by the additional parameters introduced by the latent relationships. We note that a consistent explanation for this phenomenon is that the model discovers contextual subclasses which are indicative of WordNet-type relationships. This observation opens doors to further explorations of the hypothesis regarding contextual subclasses and unsupervised relationships learning from different types of co-occurrence data.
We have presented a probabilistic generative model of words and relationships between them. By estimating the parameters of this model through stochastic gradient descent, we obtain vector and matrix representations of these words and relationships respectively. To make learning tractable, we use persistent contrastive divergence with Gibbs sampling between entity types \((S, R, T)\) to approximate gradients of the partition function. Our model uses an energy function which contains the idealised word2vec model as a special case. By augmenting the embedding space and considering relationships as arbitrary affine transformations, we combine benefits of previous models. In addition, our formulation as a generative model is distinct and allows a more flexible use, especially in the missing data, semi- and unsupervised setting. Motivated by domain-settings in which structured or unstructured data may be scarce, we illustrated how a model that combines both data sources can improve the quality of embeddings, supporting other findings in this direction.

A promising field of exploration for future work is a more detailed treatment of relationships, perhaps generalising from affine transformations to include nonlinear maps. Our choice of cosine similarity in the energy function can also be developed, as we note that this function is insensitive to very small deviations in angle, and may therefore produce looser clusters of synonyms. Nonlinearity could also be introduced in the energy, using for example splines. Furthermore, we intend to encode the capacity for richer transfer of structured information from sources such as graphs as prior knowledge into the model. Our current model can take advantage of local properties of graphs to that purpose, but has no explicit encoding for nested and distributed relationships.

A limitation of our model is its conceptual inability to embed whole sentences (which has been tackled by averaging vectors in other work, but requires deeper investigation). Recurrent or more complex neural language models offer many avenues to pursue as extensions for our model to tackle this. A particularly interesting direction to achieve that would be a combination with work such as (Jernite, Rush, and Sontag 2015), which could in principle be integrated with our model to include relationships.

The intended future application of this model is exploratory semantic data analysis in domain-specific pools of knowledge. We can do so by combining prior knowledge with unstructured information to infer, for example, new edges in knowledge graphs. A promising such field is medical language processing, retrospective exploratory data analysis may boost our understanding of the complex relational mechanisms inherent in multimodal observations, and specific medical knowledge in the form of (for example) the UMLS can be used as a strong regulariser. Indeed, initial experiments combining clinical text notes with relational data between UMLS concepts from SemMedDB (Kilicoglu et al. 2012) have demonstrated the utility of this combined approach to predict the functional relationship between medical concepts, for example, cisplatin treats diabetes. We are in the process of expanding this investigation.

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