Infrared Peak-Splitting from phonon localization in Solid Hydrogen

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The phase diagram of hydrogen is of intense interest at present as the search for crystalline metallic hydrogen hots up\textsuperscript{[1]–[5]}. Critically, metallic hydrogen must not only be made\textsuperscript{[6]}, but an unambiguous experimental signal to prove its existence is needed. It is therefore central to the endeavour that the expected spectroscopic signature is properly understood.

Due to the poor X-ray scattering and small sample sizes, precision crystallography of high pressure hydrogen has proved impossible and most information is gleaned from Raman and Infrared (IR) spectroscopy. This measures the vibrational frequencies within the crystal, and cannot determine crystal structure. However, it often provides enough information to distinguish between theoretically produced candidate structures. For this combined calculation-experiment solution of crystal structure to work, it is essential that the calculated spectra are well understood.

Because of the mass difference between the isotopes, the spectroscopic signal in hydrogen and deuterium is different. For harmonic phonons, at the same atomic volume this gives a simple frequency rescaling of $\sqrt{2}$. Variations from this give information about anharmonic behaviour, which will normally be larger for the lighter isotope. But there are practical difficulties in “equal volume” comparisons. For a given volume, the calculated pressure and free energy depend on zero point effects, which can be different in D\textsubscript{2} and H\textsubscript{2} by up to 10 GPa\textsuperscript{[7, 9]}. Volume is extremely difficult to measure experimentally, while the “diamond edge” pressure scale has been twice recalibrated by up to 20 GPa in the last ten years\textsuperscript{[10]}.

Although the H\textsubscript{2} and D\textsubscript{2} spectra are related by a simple scaling, the spectrum of hydrogen deuteride (HD) can be far more complicated. This is mainly because, once the reaction $2HD \leftrightarrow H_2 + D_2$ reaches equilibrium, the solid contains three molecular types. Molecular modes such as vibrons and rotons then split into three, while lattice modes such as layer vibration adopt an average frequency. Furthermore, because of mass-disorder, Bloch’s theorem no longer applies and the difference in masses can drive mode localization, provided the frequency is high enough\textsuperscript{[11, 12]}. These features mean that the spectroscopic signal from hydrogen-deuterium mixtures, whether Raman or IR, can look very different from the single element even if the underlying structure is identical. The importance of high frequency in allowing localization means that it is the vibron spectra where this is most pronounced\textsuperscript{[4, 12]}.

Phase III of elemental H\textsubscript{2} and D\textsubscript{2} has a particularly strong and simple IR signature\textsuperscript{[13–18]}, so it was surprising when very complex spectra were found in recent experiments starting with HD at low temperatures\textsuperscript{[1]}. At low pressures only the HD infrared peak was observed, corresponding to Phase II. Upon entering phase III, an H\textsubscript{2} peak was observed, but no D\textsubscript{2}. Subsequently two new phases were reported, based on the infrared spectra. The first transition to a new phase IV\textsuperscript{*} happened at 200 GPa where both HD and H\textsubscript{2} peak split in two and two new D\textsubscript{2} vibron peaks appeared. The second transition around 250 GPa to a phase called HD-PRE was identified by further splitting in the HD vibron.

Different phase behaviour in isotopic mixtures from pure elements is extremely difficult to understand with equilibrium thermodynamics. The electronic structure in the Born-Oppenheimer approximation is the same in each case, so isotopic differences are due to vibrational effects, notably zero point energy, which depends on mass
Density functional theory (DFT) calculations using the PBE functional have produced a range of possible candidate structures for hydrogen under these conditions, with good agreement for Raman and IR spectra of phases III and IV in pure isotopes\cite{19–25}. In calculations with static ions, DFT exhibits no isotope effects: these enter only through the vibrational behaviour, mainly zero-point effects. Spectroscopy probes this vibrational behaviour, so isotopic differences can be studied using lattice dynamics. Here we calculate the expected IR spectroscopic signature from candidate structures above 150 GPa and below room temperature.

We calculated the pressure evolution of the infrared spectra for 50:50 hydrogen-deuterium mixtures at the equilibrium concentrations of 25\% H\textsubscript{2}, D\textsubscript{2} and 50\% HD. According to now-routine calculations the energetically-favored crystal is one of a number of similar structures such as C\textsubscript{2}/c or P\textsubscript{6}\textsubscript{3}2\textsubscript{2} which can be viewed as atomic layers\textsuperscript{22,23} or as close-packed molecules\textsuperscript{20}. We choose to represent these phases with C\textsubscript{2}/c and for contrast, we also consider the C\textsubscript{mca}-12 structure, predicted to be stable at higher pressures (Fig.\textsuperscript{1}). We calculated the full Raman spectra, but we concentrate on the vibron modes because they can be directly compared with experiment (Fig.\textsuperscript{2}).

C\textsubscript{2}/c has two strongly IR-active vibron modes for pure hydrogen, which reduce in frequency with increased pressure. This unusual softening can be traced to the weakening of the covalent bond, which lengthens and loses charge as pressure increases. A cursory inspection of the full pressure dependence for C\textsubscript{2}/c (Fig.\textsuperscript{2}) shows two peaks at the onset of phase III (150 GPa), a single peak in the range 170-230 GPa, and two peaks above 250 GPa. Based only on these results, it would be easy to draw a mistaken conclusion that this peak “splitting” signified a phase transition: but since all calculations are in the same phase this can be ruled out - it is simply the effect of different pressure dependencies of the mode frequencies. To avoid this type of confusion, in this letter we draw a distinction between “peaks” - the spectroscopic observables and “modes” - their calculated cause.

Lattice dynamics in mixtures is considerably more involved than in pure elements, and we have developed sophisticated methods to tackle the problem using extended supercells (See Fig.\textsuperscript{2}\textsuperscript{11,27}). The difficulty arises because the disorder breaks translational symmetry so that crystal momentum, k, is no longer a good quantum number and the Γ-point selection rule k = 0 becomes meaningless. The twofold D/H mass difference is sufficient to cause the vibron modes to become localized. This broken symmetry confers IR activity on all modes. Comparing Fig.\textsuperscript{2}b and \textsuperscript{2}c shows that the IR activity of any individual mode in the mixture is much lower than for the Γ-point phonon in H\textsubscript{2}. So whereas the pure H\textsubscript{2} spectrum has peaks corresponding to a few unique normal modes, the peaks in the mixtures correspond to many different localized modes (c/f Fig.\textsuperscript{1}). The localised modes form three groups based on H\textsubscript{2}, HD, and D\textsubscript{2} vibrations, with each group split further due to different local environments.

Coupling between molecules causes dispersion in vibron energies. Typically, the antisymmetric IR-active modes are shifted to higher frequencies and the symmetric Raman-modes to lower frequencies. In HD mixtures, the coupling is weaker than in pure hydrogen because H\textsubscript{2} HD and D\textsubscript{2} have different resonant frequencies. So at an equivalent pressure the dispersion-like effects are smaller. Consequently strongly IR-active H\textsubscript{2}-type modes can be expected to have lower frequencies than in pure H\textsubscript{2}, while Raman frequencies for the equivalent modes in mixtures will tend to be higher. Because all modes have some IR activity, the peaks are skew with a low-frequency tail.

The H\textsubscript{2} IR vibron frequency is sometimes used experimentally to measure pressure. The different dispersion between H\textsubscript{2}-like peaks in mixtures and pure elements makes this approach unreliable.

In our isotopic mixture calculations, at low pressures, we find that the modes cluster to produce six clear distinct vibron peaks in C\textsubscript{2}/c, two for each molecular species H\textsubscript{2}, HD and D\textsubscript{2}. These modes are typically localized on one molecular type (Fig.\textsuperscript{1}). At higher pressures (above 230 GPa), we find the remarkable result that all the peaks split further, but most notably the HD signal splits into three peaks. The qualitative difference from the pure elements arises from the existence of a finite number of well-defined environments in which the molecule can find itself. This type of splitting is also observed in the C\textsubscript{mca}-12 structure.

The central result from the calculations is that the different appearance of the IR spectra in isotopic mixtures compared to pure elements is a consequence of mode localization rather the different crystal structures.

We now compare our results to the recent experiments reported by Dias et al. For convenience the main data from that paper are reproduced in the supplemental materials. Consistent with previous studies of pure H\textsubscript{2} and D\textsubscript{2} and free energy calculation assuming the C\textsubscript{2}/c structure they report the onset of phase III around 150 GPa.
The observed IR spectrum (See SM[1][27] is consistent with our lattice dynamics (Fig[1]) assuming mass scaling appropriate for HD molecules.

At around 200 GPa, Dias et al report a change in the IR spectra with new peaks appearing at frequencies consistent with Phase III of H$_2$ and D$_2$. Each of these peaks is further split, so they label this Phase HD-IV*, while noting that its phase lines are very different to the previously-named Phase IV and IV'.

We presume that this change is associated with the conversion of 2HD $\leftrightarrow$ H$_2$ + D$_2$. The equilibrium state has H and D distributed randomly between molecules, consistent with calculations showing negligible dependence of binding energy on isotope ordering[3]. After the transition from II to III, the HD dissociation might occur by lattice rebonding. Previous molecular dynamics calculations in similar layers of Phase IV have shown that the isotope-disordered equilibrium can be reached by solid-state molecular reboning effects on the picosecond timescale, albeit at higher temperatures[28][29], and that the dissociation rate increases exponentially with pressure as the bond weakens.

To compare our calculated results with experiment, we calculated phonon frequencies and IR intensities at a range of pressures from 3000 isotopically-disordered samples based on the C2/c structure. In Fig[4] we compare experimental data points [1] and calculations without making any assumption about the number of peaks in either case. Our calculations of mixtures in the C2/c phase produce peak splittings in excellent agreement with this data: $Cmca$ – 12 is significantly worse. Similar analysis has been done across a range of pressures, and by tracing the evolution it is possible to pick out persistent features. Unlike the phonons of pure hydrogen, these peaks all have similar pressure dependence. This surprising result can be traced back to the localisation of the modes, and the splitting being due to the nearby environment rather than the long range symmetry. As pressure increases stronger coupling between molecules both broadens the splitting and equalises the IR activity of the modes, making it possible to resolve the distinct local environments as seen in the HD-PRE phase. The important point is that the improved ability of resolve multiple peaks with increasing pressure does not correspond to a breaking of symmetry or to a structural phase transition.

Thus we propose that observed phases III, IV* and HD-PRE, all have the same crystal structure, probably C2/c[22] or a closely related structure[23]. The observed changes in the IR spectrum are due to isotopic effects rather than structural change. Free-energy calculations imply that III-IV* involves an isostructural 2HV $\leftrightarrow$ H$_2$ + D$_2$ equilibration reaction and that only the structure with disordered H and D atoms should appear on the equilibrium phase diagram.

As the thermodynamic equilibrium phase IV* is approached, D$_2$ molecules form and a peak corresponding to D$_2$ vibrons is observed[2]. The splitting of the IR vibron peaks in IV* is due to different modes and local environments in isotope-disordered C2/c, as opposed to the two-layer structure in Phase IV, IV' and V.

We have shown that due to mode localisation the Raman and Infrared spectra of hydrogen-deuterium mixtures are a lot more complex than those of pure isotopes, even for the same crystal structures. Moreover, under pressure the dispersion of phonon bands increases, such that vibron frequencies move further apart. So our main message is that the observation of different numbers of well-resolved peaks does not necessarily indicate a different crystal structure. This applies both to a single system under pressure, where modes have different pressure dependencies (Fig. 3) and when comparing spectra of disordered mixtures to those with a single molecular type.

These effects are sufficient to explain the multiple peaks observed in recent IR data without recourse to new crystal structures[1]. There is no reason to suppose that the equilibrium phase diagram for hydrogen-deuterium mixtures contains any phases other than those observed in pure hydrogen.

Thanks to the richness of the spectra, spectroscopic measurement with the resolution reported by Dias et al on mixtures provides important data which cannot be obtained from pure H$_2$ or D$_2$. Although spectroscopy does not provide a conclusive crystal structure determination, in combination with calculation $Cmca$–12 can be ruled out and a layered structure such as with molecules arranged close to hcp such as C2/c remains a favored candidate for Phase III[26].

Very recent work reporting cold metallic hydrogen remains controversial[10], there is no indication about the crystal structure, or even whether the sample is crystalline. This can be addressed with spectroscopy, but as yet no data is available. When it comes, the resolution is likely to be poor and interpretation difficult, and to relate it to candidate crystal structures it will be essential that it is analysed correctly as we have described. Our work here shows that studies of isotopic mixtures will provide additional information not available from pure hydrogen or deuterium, which will be crucial in finally deciphering how the long-sought Wigner-Huntingdon transition occurs.

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$^2$ we note that the experimental sample had a slight excess of hydrogen over deuterium
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FIG. 1: Upper panels show the two most intense IR-active vibron modes at 250 GPa in pure hydrogen, assuming (a) $C_2/c$ and (b) $C_{mc}$ structures (24 atoms). The unit cells comprise two layers, shown separately for clarity ($L_1$ - orange and $L_2$ - yellow). (c) Displacements corresponding to IR-active vibrons from $C_2/c$ cell (288 atoms) of disordered mixture at 250 GPa. Orange: H; cyan: D. Isotopic symmetry breaking means that all modes obtain some IR-activity. These highly localized vibron modes shown are representative examples for the spectrum generated by mixtures.

[1] R. P. Dias, O. Noked, and I. F. Silvera, Phys.Rev.Letters 116, 145501 (2016).
[2] P. Dalladay-Simpson, R. T. Howie, and E. Gregoryanz, Nature 529, 63 (2016).
[3] R. T. Howie, P. Dalladay-Simpson, and E. Gregoryanz, Nature materials 14, 495 (2015).
[4] R. T. Howie, I. B. Magdău, A. F. Goncharov, G. J. Ackland, and E. Gregoryanz, Phys. Rev. Letters 113, 175501 (2014).
[5] M. Eremets, I. Troyan, and A. Drozdov, arXiv preprint arXiv:1601.04479 (2016).
[6] R. P. Dias and I. F. Silvera, Science 355, 715 (2017).
[7] G. J. Ackland and I. B. Magdău, Cogent Physics 2, 1049477 (2015).
[8] J. McMinis, R. C. Clay III, D. Lee, and M. A. Morales, Phys.Rev.Letters 114, 105305 (2015).
[9] N. D. Drummond, B. Monserrat, J. H. Lloyd-Williams, P. L. Ríos, C. J. Pickard, and R. J. Needs, Nature communications 6 (2015).
[10] Y. Akahama and H. Kawamura, J. Phys.: Conf. Ser. 215, 012195 (2010).
[11] P. W. Anderson, Phys. Rev. 109, 1492 (1958).
[12] C. Monthus and T. Garel, Phys. Rev. B 81, 224208 (2010).
[13] R. J. Hemley and H. K. Mao, Phys.Rev.Letters 61, 857 (1988).
[14] H. E. Lorenzana, I. F. Silvera, and K. A. Goettel, Phys.Rev.Letters 63, 2080 (1989).
[15] A. F. Goncharov, E. Gregoryanz, R. J. Hemley, and H.-K. Mao, Proceedings of the National Academy of Sciences 98, 14234 (2001).
[16] P. Loubeyre, F. Occelli, and R. LeToullec, Nature 416, 613 (2002).
[17] C. S. Zha, Z. Liu, and R. J. Hemley, Phys. Rev. Letters 108, 144602 (2012).
[18] A. F. Goncharov, R. T. Howie, and E. Gregoryanz, Low Temperature Physics 39, 402 (2013).
[19] S. J. Clark, M. D. Segall, C. J. Pickard, P. J. Hasnip, M. I. Probert, K. Refson, and M. C. Payne, Zeitschrift für Kristallographie-Crystalline Materials 220, 567 (2005).
[20] J. P. Perdew, K. Burke, and M. Ernzerhof, Phys.Rev.Letters 77, 3865 (1996).
[21] C. J. Pickard and R. J. Needs, Nature Physics 3, 473 (2007).
[22] C. J. Pickard, M. Martinez-Canales, and R. J. Needs,
FIG. 2: Method used to calculate spectra in mixtures at 250 GPa from 288 atom calculations, explained in detail in SM[27].

(a) mixture data binned up in a histogram for comparison with experiment. (b) dot for the intensity of each of 144000 localized modes generated from 1000 random samples of hydrogen-deuterium mixtures. (c) IR spectrum of pure hydrogen C2/c.
FIG. 3: Stacked plot of simulated vibronic infrared signal at different pressures (shown on y-axis) for the two candidate structures $C2/c$ and $Cmca-12$. Intensities are calculated so spectra at different pressure points are comparable. On the left pure hydrogen as (a) $Cmca-12$ (b) $C2/c$. Normal-mode linewidths narrower than experimental resolution[17] are chosen to emphasize the impossibility of resolving the two $C2/c$ modes below 230 GPa. On the right we show the data for 50:50 hydrogen-deuterium mixtures (c) $Cmca-12$ (d) $C2/c$. Comparison in Fig4 (and SM) shows that $C2/c$ is a better candidate than $Cmca-12$. At low pressures $C2/c$ has six distinct peaks, two for each molecular type (H$_2$, HD, D$_2$). The two peaks per molecule type here are not connected to the distinct peaks in the pure hydrogen spectra, but rather a signature of local molecular environments. This splitting is an indirect indication of mode localization, which confers some IR activity to all modes [30].
FIG. 4: Comparison of calculated IR in $C_2/c$ mixtures (see also Fig.3) to the recent raw experimental data \[1\]. We have removed the Gaussian fits made to the data by Dias et al since this approach is invalid to describe localized modes. Theoretically calculated spectra are systematically some 200 cm$^{-1}$ softer than experimental spectra, due to a combination of errors including neglect of temperature, zero point effects in calculated pressure, calibration of the experimental pressure and choice of exchange-correlation functional \[7, 10, 30\]. (a) $C_2/c$ spectra at 300 GPa from 3000 randomized samples: gray dots are individual modes, red line is a histogram. (b) Comparison of the calculations to the digitized experimental data at 307 GPa\[1, 31\]. (c) Color map showing the calculated pressure dependence of the IR intensity compared to the equivalent experimental data\[1\].