The Impact of Accretion Disk Winds on the Optical Spectra of Cataclysmic Variables

J. H. Matthews, C. Knigge, K. S. Long, S. A. Sim, and N. Higginbottom

School of Physics and Astronomy, University of Southampton, Highfield, Southampton, SO17 1BJ, UK
Space Telescope Science Institute, 3700 San Martin Drive, Baltimore, MD 21218, USA
School of Mathematics and Physics, Queens University Belfast, University Road, Belfast, BT7 1NN, Northern Ireland, UK
Department of Astronomy, University of Las Vegas, Las Vegas, NV 89119, USA

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ABSTRACT
Many high-state non-magnetic cataclysmic variables (CVs) exhibit blue-shifted absorption or P-Cygni profiles associated with ultraviolet (UV) resonance lines. These features imply the existence of powerful accretion disk winds in CVs. Here, we use our Monte Carlo ionization and radiative transfer code to investigate whether disk wind models that produce realistic UV line profiles are also likely to generate observationally significant recombination line and continuum emission in the optical waveband. We also test whether outflows may be responsible for the single-peaked emission line profiles often seen in high-state CVs and for the weakness of the Balmer absorption edge (relative to simple models of optically thick accretion disks). We find that a standard disk wind model that is successful in reproducing the UV spectra of CVs also leaves a noticeable imprint on the optical spectrum, particularly for systems viewed at high inclination. The strongest optical wind-formed recombination lines are H\(_\alpha\) and He\(_\text{II}\) \(\lambda4686\). We demonstrate that a higher-density outflow model produces all the expected H and He lines and produces a recombination continuum that can fill in the Balmer jump at high inclinations. This model displays reasonable verisimilitude with the optical spectrum of RW Trianguli. No single-peaked emission is seen, although we observe a narrowing of the double-peaked emission lines from the base of the wind. Finally, we show that even denser models can produce a single-peaked H\(_\alpha\) line. On the basis of our results, we suggest that winds can modify, and perhaps even dominate, the line and continuum emission from CVs.

Key words: (stars:) novae, cataclysmic variables - accretion, accretion discs - stars: winds, outflows - line: profiles - radiative transfer - methods: numerical

1 INTRODUCTION
Cataclysmic variables (CVs) are systems in which a white dwarf accretes matter from a donor star via Roche-lobe overflow. In non-magnetic systems this accretion is mediated by a Keplerian disk around the white dwarf (WD). Nova-like variables (NLs) are a subclass of CVs in which the disk is always in a relatively high-accretion-rate state \((\dot{M} \sim 10^{-8} M_\odot \text{ yr}^{-1})\). This makes NLs an excellent laboratory for studying the properties of steady-state accretion disks.

It has been known for a long time that winds emanating from the accretion disk are important in shaping the ultraviolet (UV) spectra of high-state CVs \citep{1977ApJ...218L.175H,1982ApJ...255..295G}. The most spectacular evidence for such outflows are the P-Cygni-like profiles seen in UV resonance lines such as C\(_4\) \(\lambda1550\) \citep[see e.g.][for more recent results]{1982ApJ...255..295G}. Considerable effort has been spent over the years on understanding and modelling these UV features \citep[e.g.][]{1985IAUS..115....1D,1987AJ.....93..895M,1987AJ.....93.1758D,1993MNRAS.264.1011S,1995MNRAS.273..854K,1997ApJ...476..681K,1997ApJ...476..698K,2002ApJ...564..478L,2010A&A...515A..88N,2011A&A...536A..54P,2016MNRAS...455.3461P}. The basic picture emerging from these efforts is of a slowly accelerating, moderately collimated bipolar outflow that carries away \(\sim 1\% - 10\%\) of the accreting material. State-of-the-art simulations of line formation in this type of disk wind can produce UV line profiles that are remarkably similar to observations.

Much less is known about the effect of these outflows on the optical spectra of high-state CVs. These spectra are typically characterized by H and He emission lines superposed on a blue continuum. In many cases, and particularly in the SW Sex subclass of NLs \citep{1982ApJ...255..295G}.
Figure 1. Optical spectra of three nova-like variables: RW Sex (top; Beuermann et al. 1992), IX Vel (top middle; A. F. Pala & B. Matthews et al. and RW Tri were digitized from the respective publications, and the IX Vel spectrum was obtained using the XSHOOTER spectrograph T. Gaensicke, private communication) and RW Tri in and out of eclipse (bottom two panels; Groot et al. 2004). The data for RW Sex suggestion of a (potentially wind-formed) recombination continuum in the eclipsed spectrum. We have attempted to show each spectrum.

...tions in order to assess the likely impact of accretion disk's Balmer absorption edge and flatten the UV spectrum. Indeed, it has been argued that a self-consistent treatment can produce better agreement with observational data (e.g. Shaviv et al. 1991; but see also Idan et al. 2010). However, an alternative explanation, suggested by Knigge et al. (1998b; Wade 1984, 1988); Long et al. 1991, 1994; Knigge et al. 1998a) and exhibit stronger-than-observed Balmer jumps in absorption (Wadd 1984; Haardt 1987; La Dous 1989; Knigge et al. 1998b). One possible explanation for these problems is that these models fail to capture all of the relevant physics. Instead, it has been argued that a self-consistent treatment can produce better agreement with observational data (e.g. Shaviv et al. 1991; but see also Idan et al. 2010). However, an alternative explanation, suggested by Knigge et al. (1998b; Knigge et al. 1998b), is that recombination continuum emission from the base of the disk wind might fill in the disk’s Balmer absorption edge and flatten the UV spectrum.

Here, we carry out Monte Carlo radiative transfer simulations in order to assess the likely impact of accretion disk winds on the optical spectra of high-state CVs. More specifically, our goal is to test whether disk winds of the type developed to account for the UV resonance lines would also naturally produce significant amounts of optical line and/or continuum emission. In order to achieve this, we have implemented the ‘macro-atom’ approach developed by Lucy (2002, 2003) into the Monte Carlo ionization and radiative transfer code described by LK02 (a process initiated by Sim et al. 2005; hereafter SDL05). With this upgrade, the code is...
able to deal correctly with processes involving excited levels, such as the recombination emission produced by CV winds.

The remainder of this paper is organized as follows. In Section 2, we briefly describe the code and the newly implemented macro-atom approach. In Section 3, we describe the kinematics and geometry of our disk wind model. In Section 4, we present spectra simulated from the benchmark model employed by LK02, and, in Section 5, we present a revised model optimized for the optical waveband. In Section 6, we summarize our findings.

2 PYTHON: A MONTE CARLO IONIZATION AND RADIATIVE TRANSFER CODE

Python is a Monte Carlo ionization and radiative transfer code which uses the Sobolev approximation to treat line transfer (e.g. Sobolev 1957, 1960, Rybicki & Hummer 1978). The code has already been described extensively by LK02, SDL05 and Higginbottom et al. (2013; hereafter H13), so here we provide only a brief summary of its operation, focusing particularly on new aspects of our implementation of macro-atoms into the code.

2.1 Basics

Python operates in two distinct stages. First, the ionization state, level populations and temperature structure are calculated. This is done iteratively, by propagating several populations of Monte Carlo energy quanta (‘photons’) through a model wind. The geometric and kinematic properties of the outflow are specified on a pre-defined spatial grid. In each of these iterations (‘ionization cycles’), the code records estimators that characterize the radiation field in each grid cell. At the end of each ionization cycle, a new electron temperature is calculated that more closely balances heating and cooling in the plasma. The radiative estimators and updated electron temperature are then used to revise the ionization state of the wind, and a new ionization cycle is started. The process is repeated until heating and cooling are balanced throughout the wind.

This converged model is then used as the basis for the second set of iterations (‘spectral cycles’). In these, the emergent spectrum over the desired spectral range is synthesized by tracking populations of energy packets through the wind and computing the emergent spectra at a number of user-specified viewing angles.

Python is designed to operate in a number of different regimes, both in terms of the scale of the system and in terms of the characteristics of the underlying radiation field. It was originally developed by LK02 in order to model the UV spectra of CVs with a simple biconical disk wind model. SDL05 used the code to model Brackett and Pfund line profiles of H in young-stellar objects (YSOs). As part of this effort, they implemented a ‘macro-atom’ mode (see below) in order to correctly treat H recombination lines with Python. Finally, H13 used Python to model broad absorption line (BAL) QSOs. For this application, an improved treatment of ionization was implemented, so that the code is now capable of dealing with arbitrary photo-ionizing SEDs, including non-thermal and multi-component ones.

2.2 Ionization and Excitation: ‘Simple Atoms’

Prior to SDL05, the relative ionization fractions for all atomic species were estimated via the modified Saha equation (Mazzali & Lucy 1993)

\[ \frac{n_{j+1} n_e}{n_j} = W[\xi + W(1 - \xi)] \left( \frac{T_e}{T_R} \right)^{1/2} \left( \frac{n_{j+1} n_e}{n_j} \right)^* \right]. \]

(1)

Here, the ‘starred’ term on the right represents abundances computed with the Saha equation at temperature \( T_R \), but using partition functions from the dilute blackbody approximation. \( W \) is an effective dilution factor, \( \xi \) is the fraction of recombinations going directly to the ground state, and \( T_R \) and \( T_e \) are the radiation and electron temperatures, respectively. This simple ionization scheme produces reasonable results when the photoionizing SED can be approximated by a dilute blackbody. This is the case for high-state CVs. (As noted above, an improved, but more complex treatment of ionization that is appropriate for more complex SEDs is described in H13.)

Similarly, the relative excitation fractions within each ionization stage of a given species were estimated via a modified (dilute) Boltzmann equation,

\[ \frac{n_{jk}}{n_j} = \frac{W g_k}{z_j(T_R)} \exp(-E_k/kT_R), \]

(2)

where \( n_{jk} \) is the population of level \( k \) in ionic stage \( j \), \( E_k \) is the energy difference between level \( k \) and the ground state, \( g_k \) is the statistical weight of level \( k \) and \( z_j(T_R) \) is the partition function of ion stage \( j \).

Finally, Python originally modelled all bound-bound processes as transitions within a simple two-level atom (e.g. Mihalas 1982). This framework was used for the treatment of line transfer and also for the line heating and cooling calculations (see LK02). The approximation works reasonably well for resonance lines, such as C IV \( \lambda 1550 \), in which the lower level is the ground state. However, it is a poor approximation for many other transitions, particularly those where the upper level is primarily populated from above. Thus an improved method for estimating excited level populations and simulating line transfer is needed in order to model recombination lines and continua.

2.3 Ionization and Excitation: Macro-Atoms

Lucy (2002, 2003; hereafter L02, L03) has shown that it is possible to calculate the emissivity of a gas in statistical equilibrium accurately by quantising matter into ‘macro-atoms’, and radiant and kinetic energy into indivisible energy packets (r- and k-packets, respectively). His macro-atom scheme allows for all possible transition paths from a given level and provides a full non-local thermodynamic equilibrium (NLTE) solution for the level populations based on Monte Carlo estimators. The macro-atom technique has already been used to model Wolf-Rayet star winds (Sim 2004), AGN disk winds (Sim et al. 2008, Tatum et al. 2012), supernovae (Kromer & Sim 2009, Kerzendorf & Sim 2014) and YSOs (SDL05). A full description of the approach can be found in L02 and L03.

Briefly, macro-atom NLTE level populations and ionization fractions are calculated by solving the statistical equilibrium equations between each pair of levels. In the framework of the Sobolev escape probability formalism (Rybicki &
Hummer 1978; L02; Sim 2004), the bound-bound excitation rate, $R_{bl}$, in an ion is given by

$$R_{bl} = B_{bl} n_l n_e J_{est} + C_{bl} n_l n_e,$$

where $u$ and $l$ denote the upper and lower levels, $C$ represents the collisional rate coefficients, and $B$ is the usual Einstein coefficient. $J_{est}$ is the Monte Carlo estimator for the mean intensity impinging on the Sobolev region, weighted by an angle-dependent escape probability, given by (Sim 2004)

$$J_{est} = \frac{e}{4\pi \nu_0 V} \sum_i w_i \frac{1 - e^{-\tau_{sl}}}{\tau_{sl}} \frac{1}{(dv/ds)}.$$

Here $w$ is the photon weight (in luminosity units), $\nu_0$ is the line frequency, $dv/ds$ is the velocity gradient and $\tau_s$ is the Sobolev optical depth. The sum is over all photons that come into resonance with the line, and thus represents an integral over solid angle. The corresponding de-excitation rate is then

$$R_{ul} = \beta_{ul} A_{ul} n_u n_e + B_{ul} n_u J_{est} + C_{ul} n_u n_e,$$

where $\beta_{ul}$ is the angle-averaged probability that a given line photon will escape the Sobolev region.

In our implementation of the macro-atom approach, we also explicitly take into account the photoionization and collisional ionization rates between a lower level, $l$, and the continuum (or, in the case of ions with more than one bound electron, the ground state of the upper ion), $\kappa$,

$$R_{l\kappa} = n_l \int_0^\infty 4\pi J_\nu \sigma_\nu \frac{dv}{h\nu} + C_{l\kappa} n_l n_e.$$

Here, $\sigma_\nu$ is the photoionization cross section, and $J_\nu$ is the mean intensity. The corresponding recombination rate is given by

$$R_{nl} = \alpha_{nl} n_i n_e + C_{nl} n_l n_e,$$

where $\alpha_{nl}$ is the radiative recombination coefficient to level $l$. This treatment means that radiative and collisional rates to and from all levels are considered when calculating both the ionization state and the level populations, although we neglect ionization directly to excited levels of the upper ion. The van Regemorter (1962) approximation is used for collisional transitions. This means that collisions between radiatively forbidden transitions are not taken into account when one splits levels into $l$- and $s$-subshells, as well as principal quantum number, $n$ (as we have done with He i; see section 2.5). Although this approximation is, in general, a poor one, the effect is second order in the physical regime where recombination lines are formed in our models. This is because bound-free processes are dominant in determining level populations and emissivities. We have verified that this is indeed the case in the He i emission regions in our models.

2.4 Ionization and Excitation: A Hybrid Approach

SDL05 implemented a macro-atom treatment of H in PYTHON and used this to predict the observable properties of a pure H wind model for YSOs. Our goal here is to simultaneously model the optical and ultraviolet spectra of high-state CVs. Since the optical spectra are dominated by H and He recombination lines, both of these species need to be treated as macro-atoms. The UV spectra, on the other hand, are dominated by resonance lines associated with metals. This means we need to include these species in our models, but they can be treated with our (much faster) simple-atom approach. We have therefore implemented a hybrid ionization and excitation scheme into PYTHON. Any atomic species can now be treated either in our simple-atom approximation or with the full macro-atom machinery. In our CV models, we treat H and He as macro-atoms and all metals as simple-atoms. Species treated with either method are full taken into account as sources of both bound-free opacity and line opacity, and contribute to the heating and cooling balance of the plasma.

2.5 Atomic Data

We generally use the same atomic data as H13, which is an updated version of that described by LK02. In addition, we follow SDL05 in treating H as a 20-level atom, where each level is defined by the principal quantum number, $n$. For the macro-atom treatment of He, we have added the additional level and line information required from TOPBASE (Badnell et al. 2005). He I is treated in much the same way as H, but with 10 levels. He I has larger energy differentials between different $l$-subshells and triplet and singlet states. Thus, we still include levels up to $n = 10$, but explicitly treat the $l$ and $s$ sub-orbitals as distinct levels instead of assuming they are perfectly ‘l-mixed’. This allows us to model the singlet and triplet He I lines that are ubiquitous in the optical spectra of CVs (e.g. Dhillon 1996).

2.6 Code Validation and Testing

PYTHON has been tested against a number of radiative transfer and photoionization codes. LK02 and H13 conducted comparisons of ionization balance with CLOUDY (Ferland et al. 2013), demonstrating excellent agreement. We have also carried out comparisons of ionization and spectral synthesis with the supernova code TARDIS. TARDIS is described by Kerpzendorf & Sim (2014), and the spectral comparisons can be found therein. For the effort reported here, we have additionally carried out tests of the macro-atom scheme in PYTHON. Fig. 4 shows two of these tests. In the top panel, we compare the Balmer series emissivities as predicted by PYTHON in the l-mixed Case B limit against the analytical calculations by Seaton (1955). In the bottom panel, we compare PYTHON and TARDIS predictions of He I level populations for a particular test case. Agreement is excellent for both H and He.

3 DESCRIBING THE SYSTEM AND ITS OUTFLOW

PYTHON includes several different kinematic models of accretion disk winds, as well as different options for describing the physical and radiative properties of the wind-driving system under consideration. Most of these features have already been discussed by LK02 and H13, so below we only briefly recount the key aspects of the particular system and wind model used in the present study.
3.1 Wind Geometry and Kinematics

We adopt the kinematic disk wind model developed by SV93. A schematic of this model is shown in Fig. 3. In this parametrization, a smooth, biconical disk wind emanates from the accretion disk between radii $r_{\text{min}}$ and $r_{\text{max}}$. The covering fraction of the outflow is also controlled by the inner and outer opening angles of the wind, $\theta_{\text{min}}$ and $\theta_{\text{max}}$, and the launch angle of the other streamlines is given by

$$\theta(r_0) = \theta_{\text{min}} + (\theta_{\text{max}} - \theta_{\text{min}}) \left( \frac{r_0 - r_{\text{min}}}{r_{\text{max}} - r_{\text{min}}} \right)^\gamma,$$  \hspace{1cm} (8)

where $r_0$ is the launch radius of the streamline.

The poloidal (non-rotational) velocity field of the wind, $v_\phi$, is given by

$$v_\phi = v_0 + [v_\infty(r_0) - v_0] \left( \frac{l/R_\ast}{l/R_\ast + 1} \right),$$  \hspace{1cm} (9)

where $l$ is the poloidal distance along a particular wind streamline. The terminal velocity along a streamline, $v_\infty$, is set to a fixed multiple of $v_{\text{esc}}$, the escape velocity at the launch point. The launch velocity from the disk surface, $v_0$, is assumed to be constant (set to 6 km s$^{-1}$). Once the wind is launched, it accelerates, reaching half of its terminal velocity at $l = R_\ast$. The velocity law exponent $\alpha$ controls how quickly the wind accelerates. Larger values of $\alpha$ cause the main region of acceleration to occur close to $R_\ast$, whereas smaller values correspond to fast acceleration close to the disk (see Fig. 4). The rotational velocity $v_\theta$ is Keplerian at the base of the streamline and we assume conservation of specific angular momentum, such that

$$v_\theta r = v_k r_0,$$  \hspace{1cm} (10)

where $v_k = (GM/2)^{1/2}$. The density at position $(r, z)$ in the wind, $\rho(r, z)$, is calculated from the mass continuity equation, yielding

$$\rho(r, z) = \frac{r_0^2}{r} \frac{d r_0}{d r} \phi(r_0) \cos[\theta(r_0)].$$  \hspace{1cm} (11)

Here, $v_s$ is the vertical velocity component and, following SV93, $\phi(r_0)$ is the local mass-loss rate per unit area at $r_0$, defined as

$$\phi(r_0) \propto M_{\text{wind}} \cos[\theta(r_0)].$$  \hspace{1cm} (12)

We adopt $\lambda = 0$ and normalize $\phi(r_0)$ by matching its integral over both sides of the disk to the user-specified total mass-loss rate, $M_{\text{wind}}$.

3.2 Sources and Sinks of Radiation

The net photon sources in our CV model are the accretion disk, the WD and, in principle, a boundary layer with user-defined temperature and luminosity. All of these radiating bodies are taken to be optically thick, and photons striking them are assumed to be destroyed instantaneously. The
secondary star is not included as a radiation source, but is included as an occulting body. This allows us to model eclipses. Finally, emission from the wind itself is also accounted for, but note that we assume the outflow to be in radiative equilibrium. Thus all of the heating of the wind, as well as its emission, is ultimately powered by the radiation field of the net photon sources in the simulation. In the following sections, we will describe our treatment of these system components in slightly more detail.

3.2.1 Accretion Disk

**Python** has some flexibility when treating the accretion disk as a source of photons. The disk is broken down into annuli such that each annulus contributes an equal amount to the bolometric luminosity. We take the disk to be geometrically thin, but optically thick, and thus adopt the temperature profile of a standard Shakura & Sunyaev (1973) α-disk. An annulus can then be treated either as a blackbody with the corresponding effective temperature or as a stellar atmosphere model with the appropriate surface gravity and effective temperature. Here, we use blackbodies during the ionization cycles and to compute our Monte Carlo estimators. However, during the spectral synthesis stage of the simulation we use stellar atmosphere models. This produces more realistic model spectra and allows us to test if recombination emission from the wind base can fill in the Balmer jump, which is always in absorption in these models. Our synthetic stellar atmosphere spectra are calculated with Synspec\(^1\) from either Kurucz (Kurucz 1991) atmospheres (for \(T_{\text{eff}} \leq 50,000\) K) or from TLUSTY (Hubeny & Lanz 1995) models (for \(T_{\text{eff}} > 50,000\) K).

3.2.2 White Dwarf

The WD at the center of the disk is always present as a spherical occulting body with radius \(R_{\text{WD}}\) in Python CV models, but it can also be included as a source of radiation. In the models presented here, we treat the WD as a blackbody radiator with temperature \(T_{\text{WD}}\) and luminosity \(L_{\text{WD}} = 4\pi R_{\text{WD}}^2 \sigma T_{\text{WD}}^4\).

3.2.3 Boundary Layer

It is possible to include radiation from a boundary layer (BL) between the disk and the WD. In Python, the BL is described as a blackbody with a user-specified effective temperature and luminosity. In the models presented here, we have followed LK02 in setting the BL luminosity to zero. However, we have confirmed that the addition of an isotropic BL with \(L_{\text{BL}} = 0.5 L_{\text{acc}}\) and temperatures in the range 80 K \(\leq T_{\text{BL}} \leq 200\) K would not change any of our main conclusions.

3.2.4 Secondary Star

The donor star is included in the system as a pure radiation sink, i.e. it does not emit photons, but absorbs any photons that strike its surface. The secondary is assumed to be

\[^1\] http://nova.astro.umd.edu/Synspec43/synspec.html

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**Model Parameters**

| Parameter | Model A | Model B |
|-----------|---------|---------|
| \(M_{\text{WD}}\) | 0.8 \(M_\odot\) | \(10^{-8} M_\odot\) yr\(^{-1}\) |
| \(R_{\text{WD}}\) | \(7 \times 10^8\) cm | 142.9 \(R_{\text{WD}}\) |
| \(T_{\text{WD}}\) | 40,000 K | 90.4 \(R_{\text{WD}}\) |
| \(M_2\) | -0.6 \(M_\odot\) | \(10^{-9} M_\odot\) yr\(^{-1}\) |
| \(q\) | 0.75 | 12 \(R_{\text{WD}}\) |
| \(P_{\text{orb}}\) | 5.57 hr | 34.3 \(R_{\text{WD}}\) |
| \(a\) | 194.4 \(R_{\text{WD}}\) | 20.0° |
| \(R_2\) | 69.0 \(R_{\text{WD}}\) | 65.0° |
| \(V_{\text{min}}\) | 3 \(v_{\text{esc}}\) | 1 |
| \(R_v\) | 100 \(R_{\text{WD}}\) | 3 \(v_{\text{esc}}\) |
| \(\alpha\) | 1.5 | 4 |

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**Table 1.** Parameters used for the geometry and kinematics of the benchmark CV model (model A), which is optimized for the UV band, and a model which is optimized for the optical band and described in section 5 (model B). For model B, only parameters which are altered are given - otherwise the model A parameter is used. \(P_{\text{orb}}\) is the orbital period (the value for RW Tri from Walker 1963 is adopted, see section 5.4) and \(R_2\) is the radius of a sphere with the volume of the secondary’s Roche lobe. Other quantities are defined in the text or Fig. 3. Secondary star parameters are only quoted for model B as we do not show eclipses with the benchmark model (see section 5.4).

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4 A BENCHMARK DISK WIND MODEL

Our main goal is to test whether the type of disk wind model that has been successful in explaining the UV spectra of CVs could also have a significant impact on the optical continuum and emission line spectra of these systems. In order to set a benchmark, we therefore begin by investigating one of the fiducial CV wind models that was used by SV93 and LK02 to simulate the UV spectrum of a typical high-state system. The specific parameters for this model (model A) are listed in Table 1. A key point is that the wind mass-loss rate in this model is set to 10% of the accretion rate through the disk. The inner edge of the wind \((r_{\text{min}})\) is set to 4 \(R_{\text{WD}}\) following SV93. The sensitivity to some of these parameters is briefly discussed in section 5.
4.1 Physical Structure and Ionization State

Fig. 4 shows the physical and ionization structure of the benchmark disk wind model. The ionization parameter shown in the bottom right panel is given by

\[
U = \frac{4\pi}{n_H c} \int_{13.6 eV}^{\infty} \frac{J_\nu d\nu}{h\nu},
\]

where \(n_H\) is the local number density of H, and \(\nu\) denotes photon frequency. The ionization parameter is a useful measure of the ionization state of a plasma, as it evaluates the ratio of the number density of ionizing photons to the local H density.

There is an obvious drop-off in density and temperature with distance away from the disk, so any line formation process that scales as \(r^{-\beta}\) – i.e. recombination and collisionally excited emission – should be expected to operate primarily in the dense base of the outflow. Moreover, a comparison of the rotational and poloidal velocity fields shows that rotation dominates in the near-disk regime, while outflow dominates further out in the wind.

The ionization equation used in the ‘simple atom’ approach used by LK02 (see section 4) should be a reasonable approximation to the photoionization equilibrium in the benchmark wind model. Even though the macro-atom treatment of H and He does affect the computation of the overall ionization equilibrium, we would expect the resulting ionization state of the wind to be quite similar to that found by LK02. The bottom panels in Fig. 3 confirm that this is the case. In particular, He is fully ionized throughout most of the outflow, except for a small region near the base of the wind, which is shielded from the photons produced by the hot inner disk. In line with the results of LK02, we also find that CIV is the dominant C ion throughout the wind, resulting in a substantial absorbing column across a large range of velocities. As we shall see, this produces the broad, deep and blue-shifted CIV \(\lambda1550\) absorption line that is usually the most prominent wind-formed feature in the UV spectra of low-inclination nova-like CVs.
Figure 6. UV (left) and optical (right) synthetic spectra for model A, our benchmark model, computed at sightlines of 10, 27.5, 45, 62.5 and 80 degrees. The inset plots show zoomed-in line profiles for He II λ1640 and Hα. Double-peaked line emission can be seen in He II λ1640, He II λ4686, Hα and some He I lines, but the line emission is not always sufficient to overcome the absorption cores from the stellar atmosphere models. The model also produces a prominent He II λ3202 line at high inclinations.
4.2 Synthetic Spectra

We begin by verifying that the benchmark model still produces UV spectra that resemble those observed in CVs. We do expect this to be the case, since the ionization state of the wind has not changed significantly from that computed by LK02 (see section 4.1). The left column of panels in Fig. 6 shows that this expectation is met: all of the strong metal resonance lines – notably N v λ1240, Si iv λ1400 and C iv λ1550 – are present and exhibit clear P-Cygni profiles at intermediate inclinations. In addition, however, we now also find that the wind produces significant Lyα and He ii λ1640 emission lines.

Fig. 6 (right-hand panel) and Fig. 7 show the corresponding optical spectra produced for the benchmark model, and these do exhibit some emission lines associated with H and He. We see a general trend from absorption lines to emission lines with increasing inclination, as one might expect from our wind geometry. This trend is consistent with observations, as can be seen in Fig. 1. However, it is clear that this particular model does not produce all of the lines seen in observations of high-state CVs. The higher-order Balmer series lines are too weak to overcome the intrinsic absorption from the disk atmosphere, and the wind fails to produce any observable emission at low and intermediate inclinations. This contrasts with the fact that emission lines are seen in the optical spectra of (for example) V388 Sgr (Hartley et al. 2005) and IX Vel (Beuermann & Thomas 1996, see also Fig. 1).

The emissivity of these recombination features scales as $\rho^2$, meaning that they form almost entirely in the dense base of the wind, just above the accretion disk. Here, the velocity field of the wind is still dominated by rotation, rather than outflow, which accounts for the double-peaked shape of the lines. In principle, lines formed in this region can still be single peaked, since the existence of a poloidal velocity gradient changes the local escape probabilities (MC96). However, as discussed further in section 5.3, the radial velocity shear in our models is not high enough for this radiative transfer effect to dominate the line shapes.

The Balmer jump is in absorption at all inclinations for our benchmark model. This is due to the stellar atmospheres we have used to model the disk spectrum; it is not a result of photoabsorption in the wind. In fact, the wind spectrum exhibits the Balmer jump in emission, but this is not strong enough to overcome the intrinsic absorption edge in the disk spectrum. This is illustrated in Fig. 8 which shows the angle-integrated spectrum of the system, i.e. the spectrum formed by all escaping photons, separated into the disk and wind contributions. Even though the wind-formed Balmer recombination continuum does not completely fill in the Balmer absorption edge in this model, it does already contribute significantly to the total spectrum. This suggests that modest changes to the outflow kinematics might boost the wind continuum and produce emergent spectra with weak or absent Balmer absorption edges.

Figure 7. Synthetic optical spectra from model A computed for sightlines of 10, 27.5, 45, 62.5 and 80 degrees. In these plots the flux is divided by a polynomial fit to the underlying continuum redward of the Balmer edge, so that line-to-continuum ratios and the true depth of the Balmer jump can be shown.

Figure 8. Total packet-binned spectra across all viewing angles, in units of monochromatic luminosity. The thick black line shows the total integrated escaping spectrum, while the green line shows disk photons which escape without being reprocessed by the wind. The red line shows the contributions from reprocessed photons. Recombination continuum emission blueward of the Balmer edge is already prominent relative to other wind continuum processes, but is not sufficient to fill in the Balmer jump in this specific model.
5 A REVISED MODEL OPTIMIZED FOR OPTICAL WAVELENGTHS

The benchmark model discussed in section 4 was originally designed to reproduce the wind-formed lines seen in the UV spectra of high-state CVs. As we have seen, this model does produce some observable optical emission. We can now attempt to construct a model that more closely matches the observed optical spectra of CVs.

Specifically, we aim to assess whether a revised model can:

- account for all of the lines we see in optical spectra of CVs while preserving the UV behaviour;
- produce single-peaked Balmer emission lines;
- generate enough of a wind-formed recombination continuum to completely fill in the disk’s Balmer absorption edge for reasonable outflow parameters.

The emission measure of a plasma is directly proportional to its density. The simplest way to simultaneously affect the density in the wind (for fixed mass loss rate), as well as the velocity gradients, is by modifying the poloidal velocity law. Therefore, we focus on just two kinematic variables (section 3.1):

- the acceleration length, $R_v$, which controls the distance over which the wind accelerates to $\frac{v}{v_\infty}$;
- the acceleration exponent, $\alpha$, which controls the rate at which the poloidal velocity changes near $R_v$.

The general behaviour we might expect is that outflows with denser regions near the wind base – i.e. winds with larger $R_v$ and/or larger $\alpha$ – will produce stronger optical emission signatures. However, this behaviour may be moderated by the effect of the increasing optical depth through this region, which can also affect the line profile shapes. In addition, modifying $R_v$ also increases the emission volume. Based on a preliminary exploration of models with different kinematics, we adopt the parameters listed in table for our ‘optically optimized’ model (model B).

5.1 Synthetic Spectra

Fig. 11 shows the UV and optical spectra for the optically optimized model for the full range of inclinations. As expected, the trend from absorption to emission in the optical is again present, but in this revised model we produce emission lines in the entire Balmer series at high inclinations, as well as the observed lines in He ii and He i. This can be seen more clearly in the continuum-normalized spectrum in Fig. 10.

Two other features are worth noting in the optical spectrum. First, the collisionally excited Ca ii emission line at 3934 Å becomes quite prominent in our densest models. Second, our model predicts a detectable He ii recombination line at 3202 Å. This is the He equivalent of Paschen $\beta$ and should be expected in all systems that feature a strong He ii $\lambda 4686$ line (the He equivalent of Paschen $\alpha$). This line is somewhat unfamiliar observationally, because it lies bluewards of the atmospheric cut-off, but also redwards of most ultraviolet spectra.

Our models do not exhibit P-Cygni profiles in the optical lines. This is perhaps not surprising. LK02 and SV93 originally designed such models to reproduce the UV line profiles. Thus, most of the wind has an ionization parameter of $\log U \sim 2$ (see Fig. 5). This means H and He are fully ionized throughout much of the wind and are successful in producing recombination features. However, the line opacity throughout the wind is too low to produce noticeable blue shifted absorption. We suspect that the systems that exhibit such profiles must possess a higher degree of ionization stratification, although the lack of contemporary observations means it is not known for certain if the P-Cygni profiles in UV resonance lines and optical H and He lines exist simultaneously. Ionization stratification could be caused by a clumpy flow, in which the ionization state changes due to small scale density fluctuations, or a stratification in density and ionizing radiation field over larger scales. Invoking clumpiness in these outflows is not an unreasonable hypothesis. Theories of line-driven winds predict an unstable flow (MacGregor et al. 1974; Owocki & Rybicki 1984, 1985), and simulations of CV disk winds also produce density inhomogeneities (Proga et al. 1998, 2002). Tentative evidence for clumping being directly related to P-Cygni optical lines comes from the fact that Prinja et al. (2000) found the dwarf nova BZ Cam’s outflow to be unsteady and highly mass-loaded in outburst, based on observations of the UV resonance lines. This system has also exhibited P-Cygni profiles in He i $\lambda 5876$ and H$\alpha$ when in a high-state (Patterson et al. 1995; Ringwald & Navloj 1999). The degree of ionization and density variation and subsequent line opacities may be affected by our model parameters and the specific parameterization we have adopted.

In the UV, the model still produces all the observed lines, and deep P-Cygni profiles are produced in the normal resonance lines, as discussed in section 4.2. However, the UV spectra also display what is perhaps the biggest problem with this revised model, namely the strength of resonance line emission at low and intermediate inclinations. In order to generate strong optical wind signatures, we have adopted wind parameters that lead to very high densities at the base of the wind ($n_e \sim 10^{13} - 10^{14}$ cm$^{-3}$). This produces the desired optical recombination emission, but also increases the role of collisional excitation in the formation of the UV resonance lines. This explains the pronounced increase in the emission component of the Crv A1550 resonance line, for example, relative to what was seen in the benchmark model (compare Figures 6 and 7). The strength of this component in the revised model is probably somewhat too high to be consistent with UV observations of high-state CVs (see e.g. Long et al. 1991, 1994; Noebauer et al. 2010).

5.2 Continuum Shape and the Balmer Jump

The wind now also has a clear effect on the continuum shape, as shown by Fig. 11. In fact, the majority of the escaping spectrum has been reprocessed in some way by the wind, either by electron scattering (the wind is now moderately Thomson-thick), or by bound-free processes. This is demonstrated by the flatter spectral shape and the slight He photoabsorption edge present in the optical spectrum (marked in Fig. 10). This reprocessing is also responsible for the change in continuum level between models A and B. In addition, Figures 8, 10 and 11 clearly demonstrate that the wind produces a recombination continuum sufficient to
**Figure 9.** UV (left) and optical (right) synthetic spectra for model B computed at sightlines of 10, 27.5, 45, 62.5 and 80 degrees. Model A is shown in grey for comparison. The inset plots show zoomed-in line profiles for He II λ1640 and Hα. The Balmer and He are double-peaked, albeit with narrower profiles. Strong He II λ4686 emission can be seen, as well as a trend of a deeper Balmer jump with decreasing inclination.
completely fill in the Balmer jump at high inclinations. This might suggest that Balmer continuum emission from a wind can be important in shaping the Balmer jump region, as originally suggested by Knigge et al. (1998b; see also Hassall et al. 1985).

It should be acknowledged, however, that the Balmer jump in high-state CVs would naturally weaken at high inclinations due to limb darkening effects (La Dous 1989a, b). Although we include a simple limb darkening law which affects the emergent flux at each inclination, we do not include it as a frequency dependent opacity in our model. As a result, the efficiency of filling in the Balmer jump should really be judged at low and medium inclinations, where, although prominent, the recombination continuum does not overtake the disk atmosphere absorption. In addition, this effect could mean that any model which successfully fills in the jump at low inclinations could lead to a Balmer jump in emission at high inclinations. In any case, to properly understand this phenomenon, a fully self-consistent radiative transfer calculation of both the disk atmosphere and connected wind is required.

5.3 Line Profile Shapes: Producing Single-Peaked Emission

Fig. 12 shows how the Hα profile changes with the kinematics of the wind for an inclination of 80°. The main prediction is that dense, slowly accelerating wind models produce narrower emission lines. This is not due to radial velocity shear. As stated by MC96, that mechanism can only work if poloidal and rotational velocity gradients satisfy \( (dv_\phi/dr)/(dv_\phi/dr) \gtrsim 1 \); in our models, this ratio is always \( \lesssim 0.1 \). Instead, the narrow lines predicted by our denser wind models can be traced to the base of the outflow becoming optically thick in the continuum, such that the line emission from the base of the wind cannot escape to the observer. In such models, the ‘line photosphere’ (the \( \tau \approx 1 \) surface of the line-forming region) moves outwards, towards larger vertical and cylindrical distances. This reduces the predicted line widths, since the rotational velocities – which normally provide the main line broadening mechanism at high inclination – drop off as \( 1/r \). This is not to say that the MC96 mechanism could not be at work in CV winds. For example, it would be worth investigating alternative prescriptions for the wind velocity field, as well as the possibility that the outflows may be clumped. An inhomogeneous flow (which has been predicted in CVs; see section 5.2) might allow large radial velocity shears to exist while still maintaining the high densities needed to produce the required level of emission. However, such an investigation is beyond the scope of the present paper.

In our models, single-peaked line profiles are produced once the line forming region has been pushed up to ~ \( 10^{11} \) cm (~ 150 \( R_{WD} \)) above the disk plane. This number may seem unrealistically large, but the vertical extent of the emission region is actually not well constrained observationally. In fact, multiple observations of eclipsing NLS show that the Hα line is only moderately eclipsed compared to the continuum (e.g. Baptista et al. 2000; Groot et al. 2004; see also section 5.4), implying a significant vertical extent for the line-forming region. This type of model should therefore not be ruled out a priori, but this specific model was not adopted as our optimally optimized model due to its unrealistically high continuum level in eclipse.

5.4 Sensitivity to Parameters

This revised model demonstrates that one can achieve a more realistic optical spectrum by altering just two kinematic parameters. However, it may also be possible to achieve this by modifying other free parameters such as \( M_{\text{accr}} \), the opening angles of the wind and the inner and outer launch radii. For example, increasing the mass loss rate of the wind increases the amount of recombination emission (which scales as \( \rho^2 \)), as well as lowering the ionization parameter and increasing optical depth through the wind. Wider launch radii and opening angles lead to a larger emitting volume, but this is moderated by a decrease in density for a fixed mass-loss rate. We also note that the inner radius of 4 \( R_{WD} \) adopted by SV93 affects the emergent UV
velocity shear (see section 5.3). and a single-peaked line in model X. This is not due to radial acceleration length of $R$ and $B$ respectively, and a third model (X) which has an increased improved optical model described in section 6 are labeled as A and B respectively, and a third model (X) which has an increased acceleration length of $R_0 = 283.8 \, R_{WD}$, and $\alpha = 4$ is also shown. The $x$-axis limits correspond to the Keplerian velocity at $4R_{WD}$, the inner edge of the wind. We observe a narrowing of the lines, but the effect on the optical spectrum is negligible. We have verified this general behaviour, but we suggest that future work should investigate the effect of these parameters in more detail as well as incorporating a treatment of clum-}

If a wind really does produce the line and continuum emission seen in optical spectra of high-state CVs, then understanding the true mass loss rate and geometry of the outflow is clearly important.

5.5 Comparison to RW Tri

Fig. 13 shows a comparison of the predicted out-of-eclipse and mid-eclipse spectra against observations of the high-inclination nova-like RW Tri. The inclination of RW Tri is somewhat uncertain, with estimates including 70.5° (Smak 1993), 75° (Groot et al. 2004), 80° (Longmore et al. 1981) and 82° (Frank & King 1981). Here, we adopt $i = 80°$, but our qualitative conclusions are not particularly sensitive to this choice. We follow LK02 is setting the value of $\tau_{disk}$ (the maximum radius of the accretion disk) to $34.3 \, R_{WD}$. When compared to the semi-major axis of RW Tri, this value is perhaps lower than one might typically expect for NLs (Harrop-Allin & Warner 1996). However, it is consistent with values inferred by Rutten et al. (1992). We emphasize that this model is in no sense a fit to this – or any other – data set.

The similarity between the synthetic and observed spectra is striking. In particular, the revised model produces strong emission in all the Balmer lines, with line-to-continuum ratios comparable to those seen in RW Tri. Moreover, the line-to-continuum contrast increases during eclipse, as expected for emission produced in a disk wind. This trend is in line with the observations of RW Tri, and it has also been seen in other NLs, including members of the SW Sex class (Neustroev et al. 2011). As noted in section 5.2, the majority of the escaping radiation has been reprocessed by the wind in some way (particularly the eclipsed light).

However, there are also interesting differences between the revised model and the RW Tri data set. For example, the model exhibits considerably stronger He II features than the observations, which suggests that the overall ionization state of the model is somewhat too high. As discussed in section 5.3, the optical lines are narrow, but double-peaked. This is in contrast to what is generally seen in observations of NLs, although the relatively low resolution of the RW Tri spectrum makes a specific comparison difficult. In order to demonstrate the double-peaked nature of the narrower lines, we choose not to smooth the synthesized data to the resolution of the RW Tri dataset. If the data was smoothed, the Hα line would appear single-peaked.

6 CONCLUSIONS

We have investigated whether a disk wind model designed to reproduce the UV spectra of high-state CVs would also have a significant effect on the optical spectra of these systems. We find that this is indeed the case. In particular, the model wind produces H and He recombination lines, as well as a recombination continuum blueward of the Balmer edge. We do not produce P-Cygni profiles in the optical H and He lines, which are seen in a small fraction of CV optical spectra. Possible reasons for this are briefly discussed in section 5.2. We have also constructed a revised benchmark model...
which is designed to more closely match the optical spectra of high-state CVs. This optically optimized model produces all the prominent optical lines in and out of eclipse, and achieves reasonable verisimilitude with the observed optical spectra of RW Tri. However, this model also has significant shortcomings. In particular, it predicts stronger-than-observed He \textsc{ii} lines in the optical region and too much of a collisionally excited contribution to the UV resonance lines.

Based on this, we argue that recombination emission from outflows with sufficiently high densities and/or optical depths might produce the optical lines observed in CVs, and may also fill in the Balmer absorption edge in the spectrum of the accretion disk, thus accounting for the absence of a strong edge in observed CV spectra. In section 5.3, we demonstrate that although the double peaked lines narrow and single-peaked emission can be formed in our densest models, this is not due to the radial velocity shear mechanism proposed by MC96. We suggest that ‘clumpy’ line-driven winds or a different wind parameterization may nevertheless allow this mechanism to work. We also note the possibility that, as in our denser models, the single-peaked lines are formed well above the disk, where rotational velocities are lower.

It is not yet clear whether a wind model such as this can explain all of the observed optical features of high-state CVs – further effort is required on both the observational and modelling fronts. However, our work demonstrates that disk winds matter. They are not just responsible for creating the blue-shifted absorption and P-Cygni profiles seen in the UV resonance lines of high-state CVs, but can also have a strong effect on the optical appearance of these systems. In fact, most of the optical features characteristic of CVs are likely to be affected – and possibly even dominated – by their disk winds. Given that optical spectroscopy plays the central role in observational studies of CVs, it is critical to know where and how these spectra are actually formed. We believe it is high time for a renewed effort to understand the formation of spectra in accretion disks and associated outflows.

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