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Financial earthquakes: SARS-CoV-2 news shock propagation in stock and sovereign bond markets

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Abstract

The SARS-CoV-2 epidemics outbreak has shocked global financial markets, inducing policymakers to put in place unprecedented interventions to inject liquidity and to counterbalance the negative impact on worldwide financial systems. Through the lens of statistical physics, we examine the financial volatility of the reference stock and bond markets of the United States, United Kingdom, Spain, France, Germany and Italy to quantify the effects of country-specific socio-economic and political announcements related to the epidemics. Main results show that financial markets exhibit heterogeneous behaviours towards news on the epidemics, with the Italian and German bond markets responding with major delays to shocks. Additionally, credit markets tend to be slower than equity markets in adjusting prices after shocks, hence being slower at incorporating the effects of such news.

1. Introduction

The spread of the novel coronavirus (SARS-CoV-2) has posed unprecedented economic and financial turmoils in most of the countries, representing a massive geo-economic shock to the worldwide economy. Starting from China, the shock expanded to the international scene hitting financial markets all over the globe. During the period ranging from 20 February 2020 to 20 March 2020, the US S&P 500 lost as much as 31.7%, whereas the UK FTSE 100 dropped by 30.2%. The Euro area saw its financial markets severely plummeting as well, with the German DAX index declining by 49.3%, the Italian FTSE MIB losing 37.3%, and the Spanish IBEX 35 dropping of as much as 35.1%. Also government bond markets have been massively impacted as a consequence of the epidemic spread: the 1-Year US Treasury securities yield declined from 1.47 to 0.14 – a 90.5% drop – whereas the UK 1-Year bond yield saw its value decreasing from 0.635 to 0.083 – an almost 87% negative yield. Worldwide governments, along with central banks, have put in place unprecedented recovery plans to cope with the economic impact of the pandemic.

Besides studying the effects of the pandemic on the real economy (see e.g. [1]), several researchers have recently investigated the impact of official announcements regarding SARS-CoV-2 on global financial markets, highlighting the
role of the pandemic as a source of financial volatility, and that of response policies as potential spreaders of further uncertainties into global financial markets (see, e.g., [2–6]). Although there is a general attention to equity market reactions, the impact and persistence analysis of equity and government bond market volatility shocks induced by SARS-CoV-2 related announcements is still an open question.

SARS-CoV-2 news can be regarded as earthquake mainshocks, whose associated foreshocks and aftershocks impact the volatility dynamics of financial markets. Pre-shock and aftershock rates and intensities can be described by several widely known empirical laws, such as the Omori law. According to the Omori law, aftershock rates decrease over time roughly by the reciprocal of time which follows the earthquake mainshock. In the context of financial markets, Sornette et al. [7] studied the behaviour of the S&P 500 index before and after the Black Monday of 19 October 1987, finding that the implied market volatility after the market crash has follows a power-law with a log-periodic rate of decay. The studies of Lillo and Mantegna [8,9] on the NYSE in the neighbourhood of the Black Monday crash find evidence on the fact that the rate of extreme volatility spikes follows a power-law that is equivalent to the modified Omori law. The applications of [10–12] on several stock market indices showed how the non-linearity of the return and volatility distributions of stock indices before and after a shock allows to employ the Omori law to describe the volatility outburst, as well as that the memory in volatility is induced not only by the main crashes, but also by sub-crashes.

Against this background, we investigate the impact of SARS-CoV-2 related news on major equity and bond markets through the lens of seismology (see [13,14]), deriving parallels between energy dissipation and market volatility cascades. In the context of asset price perturbations (see e.g. [15–18]), we employ the Omori law, which characterizes the non-stationary phase observed in the neighbourhood of an earthquake, to study the foreshock and aftershock dynamics of financial systems agitated by the occurrence of extreme events related to the epidemics. Additionally, we study the relationship between the mainshocks and their largest aftershocks through Bath’s law. Previous research on the relaxation dynamics of financial markets after crashes has shown that the power-law tail is adequate in describing their volatility patterns after major shocks (see, for instance, [8–10,19–22]).

Earthquakes are prominent examples of complex phenomena showing scale-invariance and fractality properties, prominent features which have been frequently observed in financial market data (see [23–26]). The emergence of these properties is an indication of complexity and nonlinear dynamics in the context of the earthquake generation process. News effects can be conceived as earthquakes, which shock financial markets with a mainshock propagating across venues over time. Further, they can generate aftershocks, which indicate that the market is still discounting the news effects over time. This is in line with the extant literature investigating financial market crashes as earthquakes (see, for instance, [12,27–34]).

We study the country-specific effects of socio-economic and political news, including financial stimulus announcements, on a group of representative countries, whose financial systems have been significantly impacted by the evolution of the epidemics, over the period from January 2020 to April 2020. In other words, we investigate cascade effects on the volatility patterns of the reference equity market of the US (S&P500), the UK (FTSE100), Spain (IBEX35), France (CAC40), Germany (DAX) and Italy (FTSE-MIB) and of each country’s 1-Year bond yield. This allows us to determine which markets are more efficient at incorporating SARS-CoV-2 related news and to characterize which is their foreshock and aftershock dynamics towards such exogenous shocks.

Our approach can be extended and integrated in a multivariate setting with the statistical and econometric framework on interconnectedness, systemic risk and spillover measurement. The information shares developed by Hasbrouck [35] and the common factor components of [36] have been widely employed in the empirical literature – see, for instance, Mizrahi and Neely [37], Pagnottoni and Dimpfl [38], Grammig and Peter [39]. Additionally, the systemic risk and spillover framework proposed by Diebold and Yilmaz [40], Diebold and Yilmaz [41] has given rise to a variety of financial applications – e.g. [42–45]. Possible extensions of the work might also involve alternative econometric measures of connectedness as in [46], systemic risk measures as in [47], and news contagion risk as in [48]. Such approaches could unveil relevant information on the interaction of different markets when common shocks occur.

The paper proceeds as follows. Section 2 introduces the Omori law and its linkage with the financial volatility dynamics. Section 3 presents and discusses the results. Section 4 concludes.

2. Methodology

Let us denote the time of announcement of a generic SARS-CoV-2 related event as \( T_s \). We aim at studying the decay of massive volatility fluctuations in the \( k \) days before and after the announcement date \( T_s \), which we set at \( k = 10 \) days in the present context. Denoting the price of the generic asset (equity or bond yield) \( i \) at time \( t \) as \( p_i(t) \), we determine the daily market volatility of as:

\[
V_i(t) = |\log(p_i(t)) - \log(p_i(t - 1))|. 
\]

We consider the 10-base logarithm scale as frequently done in seismology. This is because the number of aftershocks which follow an earthquake mainshock has been shown to be linearly dependent on displacement time when represented in its 10-base logarithm scale (see [14]).
From Eq. (1), denoting as \( q_i \) the value of the \( q \)th percentile\(^1\) of the volatility distribution of the time series \( i \), we derive the correspondent binary volatility time series \( n_i(t) \) as:

\[
n_i(t) = \begin{cases} 
1, & V_i(t) \geq q_i \\
0, & V_i(t) < q_i. 
\end{cases}
\]

In other words, in this way we investigate the number of times a volatility time series assumes larger values than the considered threshold. This is equivalent to study the number of aftershocks measured at time \( t \) after the earthquake’s mainshock. The choice of selecting a threshold to compute the binary volatility series is in accordance with previous related research (see [11,20,21,49]). Furthermore, [8,9] show that, in the aftermath of a market crash, the volatility can be represented as a stochastic process with a power-law decay rate, which makes pure autoregressive models, such as GARCH models, less adequate in describing the observed aftershock volatility dynamics.

We then study the response of financial and bond markets to SARS-CoV-2 related news through tools developed in the field of seismology. Specifically, we provide parallels between the energy relaxation process occurring after main shocks in the context of earthquakes and the market volatility cascades generated by SARS-CoV-2 related announcements. The Omori law [14] provides a theoretical framework for quantifying the magnitude of pre- and after-shock volatility decays in time (see, for instance, [20,21,50,51]), as well as it detects statistical regularities in geophysical earthquakes (see [13]). Indeed, as per the Omori law, the number of after-shock earthquakes per unit time, measured at time \( t \), decays following a power law. In other words, the rate of high volatility counts \( N(t) \) following a single perturbation at time \( T_s \) is given by:

\[
N_i(|t - T_s|) \sim |t - T_s|^{-\beta_{Ni}}
\]

where \( \beta_{Ni} \) is the parameter representing the Omori power law exponent, and \( N_i(t) = \frac{1}{H} \sum_{j=1}^{H} n_{ij}(t) \) is the average rate of high volatility occurrences induced by the set of \( H \) events in the generic asset \( i \). With the aim of estimating the power law relationship between high volatility regimes and displacement time \( \tau = |t - T_s| \), we derive the cumulative number of events above the threshold \( q \) at time \( t \) as:

\[
\Phi_i(|t - T_s|) = \int_{T_s}^{t} N_i(|t' - T_s|)dt' \propto |t - T_s|^{-\beta_{Ni}}
\]

Then, we compare the volatility dynamics preceding and following SARS-CoV-2 related events by discerning between \( N_i^{{Pre}}(t|t < T_s) \) and \( N_i^{{Aft}}(t|t < T_s) \). Finally, by performing an ordinary least square estimation on a log–log scale we derive the pre- and after-shock Omori power-law exponents, denoted as \( \beta_{Ni}^{{Pre}} \) and \( \beta_{Ni}^{{Aft}} \), respectively.

The Omori exponents are useful to quantify volatility reactions to SARS-CoV-2 related news. The higher the Omori exponents, the faster the reaction of the market to SARS-CoV-2 announcements – during the foreshock phase – and absorption of the shock – during the aftershock phase – are. Conversely, the lower the exponents, the slower the shock is perceived by the market – during the foreshock phase – and the more relaxed the market comes back to its equilibrium state after the shock has occurred – during the aftershock phase.

We illustrate the previously discussed concept in Fig. 1, which gives an overview of the interpretation of the Omori exponents. To this aim, we simulate 1000 power law realizations with two representative \( \beta \) parameters, equal to 0.2 and 0.1, for 20 points in time (comprising the foreshock and aftershock period). We average across the simulated distributions and obtain the volatility distributions illustrated in the main panel of Fig. 1. Notice how the simulated volatility distribution with \( \beta \) equal to 0.2 is more peaked towards the event date than that having a \( \beta \) of 0.1, with a faster relaxation dynamics both during the pre-shock and after-shock periods. We then represent the cumulative distribution function from \( t_0 = 0 \) backwards (foreshock) and that from \( t_0 \) onwards (after shock) for the two power law distributions. The different “V” shapes and, in particular, the inclinations of the cumulative distribution functions indicate that a higher power law exponent corresponds to a faster volatility decay.

In addition, it is worth investigating the relationship between the size of the largest shock \( V_1 = V(T_c) \) and that of the second one \( V_2 \), both before and after \( T_c \). For this purpose, the Bath law parameter, which we denote as \( B \), expresses the relation between \( V_1 \) and \( V_2 \), i.e.

\[
M_1 - M_2 = \log_{10}(V_1) - \log_{10}(V_2) = B
\]

The aforementioned functional form implies the following relationship between the two volatility shocks:

\[
V_2/V_1 = C_B
\]

and, thus, \( B = -\log_{10}C_B \).

\(^1\) We consider the 85-th percentile of the volatility distribution as a threshold to classify the volatility series outburst and the volatility regimes in regular background activity.
Fig. 1. Simulated volatility patterns and Omori exponents. The main panel shows the simulated volatility patterns for two different power laws with $\beta$ equal to 0.2 (in blue) and 0.1 (in red). The inset illustrates the dynamics of the cumulative distribution function from $t_0 = 0$ backwards (foreshock) and that from $t_0$ onwards (after shock) for the two power law distributions.

Table 1 United States SARS-CoV-2 related events. The table shows major SARS-CoV-2 related events in the United States during the period 20 January 2020–30 April 2020.

| Date     | Event Description                                                                 |
|----------|-----------------------------------------------------------------------------------|
| 20/01/20 | First confirmed case.                                                             |
| 29/02/20 | First reported death.                                                             |
| 11/03/20 | The World Health Organization’s Director-General declares that COVID-19 can be characterized as a pandemic. |
| 13/03/20 | Approval of an aid economic package for workers and individuals.                   |
| 16/03/20 | Trump issues guidelines to avoid social gatherings and to restrict discretionary travels. |
| 22/03/20 | Trump announces the approval of Washington emergency declaration.                  |
| 24/03/20 | The White House and Senate leaders of both parties announced agreement of a $2 trillion measure to aid workers, businesses and the healthcare system. |
| 06/04/20 | The Federal Reserve announces it will support banks that lend to small businesses. |
| 14/04/20 | The International Monetary Fund estimates global GDP to decline of about 3%.         |
| 15/04/20 | Trump announces guidelines on reopening the US economy.                            |

3. Empirical results

As a preliminary analysis, we compare the volatility patterns of each country equity index and bond yield series in the neighbourhood of SARS-CoV-2 related news. A comprehensive list of the considered country-specific events can be found in Tables 1–6. We select major events related to the evolution of the epidemics between January 2020, when the first cases manifested, and the end of April 2020, thus including the majority of the first wave of lockdown and mobility restriction measures, the announcements of economic aid packages (both from single countries and supranational authorities), and the lockdown lifting decisions.

Fig. 2 shows that the largest part of the SARS-CoV-2 related events is concentrated around the middle of March, when lockdown and intervention policies were globally put in place, and in April, when governments’ reaction plans have been announced and major economic outlooks released. Notice that equity and bond markets have a different reaction to SARS-CoV-2 news. Volatility series of equity indices peak on March 11th, when the World Health Organization recognized SARS-CoV-2 as a pandemic (see [52]), while bond yields present a greater reaction during macroeconomic announcements, such as on 23 March when the European Commission announced a financial aid package of 750 bln Euros to mitigate the negative economic consequences of SARS-CoV-2 outbreak, and on 14 April when the IMF negative World Economic Outlook was released (see [53]).

From Fig. 3 we notice that the volatility dynamics of equity markets are highly correlated, with a lower bound of 0.689, which represents the Pearson correlation coefficient between the S&P500 and the FTSE-MIB, and an upper bound of 0.9562 between CAC40 and DAX, whereas bond yields volatility correlations are less pronounced during the same period, exhibiting even negative values.
Table 2
Germany SARS-CoV-2 related events. The table shows major SARS-CoV-2 related events in Germany during the period 20 January 2020–30 April 2020.

| Date         | Event                                                                 |
|--------------|-----------------------------------------------------------------------|
| 25/02/2020   | First confirmed cases in the Baden–Württemberg region.               |
| 09/03/2020   | First reported death.                                                 |
| 10/03/2020   | Merkel announces up to 70% of Germany could become infected.          |
| 11/03/2020   | Merkel announces liquidity support for companies.                     |
| 17/03/2020   | The World Health Organization's Director-General declares that COVID-19 can be characterized as a pandemic. |
| 23/03/2020   | The health threat switches from moderate to high.                     |
| 24/03/2020   | The European Commission approves, under the Temporary Framework, a German scheme to support companies. |
| 01/04/2020   | Social distancing measures are extended until April 19th.             |
| 09/04/2020   | The ministers of Finances of the Eurozone countries agreed to a €500 billions aid, including the possibility of using the European Stability Mechanism. |
| 14/04/2020   | The International Monetary Fund estimates global GPD to decline of about 3%. |
| 23/04/2020   | The European Council approves a financial aid package worth €540 billions. |
| 30/04/2020   | The European Central Bank announces new pandemic emergency longer-term refinancing operations. |

Table 3
France SARS-CoV-2 related events. The table shows major SARS-CoV-2 related events in France during the period 20 January 2020–30 April 2020.

| Date         | Event                                                                 |
|--------------|-----------------------------------------------------------------------|
| 24/01/2020   | First confirmed case.                                                 |
| 14/02/2020   | First reported death.                                                 |
| 10/03/2020   | Introduction of mobility and activities restrictions.                 |
| 11/03/2020   | The World Health Organization's Director-General declares that COVID-19 can be characterized as a pandemic. |
| 16/03/2020   | Announcement of national lockdown.                                    |
| 17/03/2020   | The French Finance Minister Le Maire announces a €45 billions aid package for small businesses and other hard-hit sectors. |
| 24/03/2020   | The European Commission approves, under Article 107(3)(b), three French State aid schemes. |
| 14/04/2020   | The International Monetary Fund estimates global GPD to decline of about 3%. |
| 23/04/2020   | The European Council approves a financial aid package worth €540 billions. |
| 28/04/2020   | The Prime Minister reveals plans to ease SARS-CoV-2 lockdown measures. |
| 30/04/2020   | The European Central Bank announces new pandemic emergency longer-term refinancing operations. |

Table 4
Spain SARS-CoV-2 related events. The table shows major SARS-CoV-2 related events in Spain during the period 20 January 2020–30 April 2020.

| Date         | Event                                                                 |
|--------------|-----------------------------------------------------------------------|
| 31/01/2020   | First confirmed case.                                                 |
| 12/02/2020   | First reported death.                                                 |
| 09/03/2020   | State of emergency declaration in the community of Madrid.            |
| 10/03/2020   | The European Commission proposes to “free up €7.5 billions of liquidity”. |
| 11/03/2020   | The World Health Organization’s Director-General declares that COVID-19 can be characterized as a pandemic. |
| 13/03/2020   | The state of emergency is extended to the whole country.              |
| 17/03/2020   | Announcement of a €200 billions support package.                      |
| 22/03/2020   | Lockdown measures are extended until April 11th.                      |
| 24/03/2020   | G7 finance ministers and central bank governors meeting, pledging to do “whatever is necessary” to help their economies recover from the coronavirus. |
| 09/04/2020   | The ministers of Finances of the Eurozone countries agree to a €500 billions aid, including the possibility of using the European Stability Mechanism. |
| 14/04/2020   | Adoption of some gradual measures for easing the lockdown.            |
| 23/04/2020   | The European Council approves a financial aid package worth €540 billions. |
| 28/04/2020   | Unveiling of a gradual exit strategy from lockdown.                   |
| 30/04/2020   | The European Central Bank announces new pandemic emergency longer-term refinancing operations. |

In Fig. 4 we show the volatility distributions of equity indices and bond yields along with their 85-th percentiles taken as a benchmark for large volatility deviations. The figure confirms that, overall, we do isolate normal background activity of financial volatilities with the choice of our percentile, therefore ensuring we are taking into account only for extreme values of the financial time series.

Fig. 5 illustrates how SARS-CoV-2 related news impacted the volatility fluctuations of equity and bond markets both during the pre-shock and after-shock phases. In particular, the upper panels show the average empirical cumulative distribution function (CDF) of abnormal volatility movements preceding and following major SARS-CoV-2 news for the
Table 5
Italy SARS-CoV-2 related events. The table shows major SARS-CoV-2 related events in the Italy during the period 20 January 2020–30 April 2020.

| Date       | Event Description                                                                 |
|------------|-----------------------------------------------------------------------------------|
| 31/01/2020 | First confirmed cases in Rome (Chinese couple).                                    |
| 20/02/2020 | First confirmed case in Codogno.                                                   |
| 22/02/2020 | First death in Veneto and creation of the first “red zones” in Lombardy and Veneto. |
| 09/03/2020 | Declaration of national lockdown.                                                   |
| 10/03/2020 | The European Commission proposes to “free up €7.5 billions of liquidity”.          |
| 11/03/2020 | Further restrictions on lockdown related to travel and approval of a €25 billions financial package. |
| 21/03/2020 | Halt to all non-essential production activities.                                  |
| 24/03/2020 | G7 finance ministers and central bank governors meeting, pledging to do “whatever is necessary” to help their economies recover from the coronavirus. |
| 06/04/2020 | Announcement of an economic stimulus worth €200 billions.                          |
| 09/04/2020 | The ministers of Finances of the Eurozone countries agreed to €500 billion aid, including the possibility of using the ESM. |
| 10/04/2020 | Declaration of national lockdown.                                                   |
| 11/04/2020 | The European Council approves a financial aid package worth €540 billions.          |
| 14/04/2020 | Conversion of the “Cura Italia” decree into law.                                  |
| 23/04/2020 | The government introduces the Coronavirus Bill 2019–21.                            |
| 28/04/2020 | The Office for Budget Responsibility publishes a scenario under which UK GDP would fall by 35% in the second quarter of 2020. The International Monetary Fund estimates global GPD to decline of about 3%. |

Table 6
United Kingdom SARS-CoV-2 related events. The table shows major SARS-CoV-2 related events in the United Kingdom during the period 20 January 2020–30 April 2020.

| Date       | Event Description                                                                 |
|------------|-----------------------------------------------------------------------------------|
| 31/01/2020 | First confirmed cases.                                                            |
| 11/03/2020 | The World Health Organization’s Director-General declares that COVID-19 can be characterized as a pandemic. |
| 12/03/2020 | The Chief Medical Officers raises the risk for the UK from moderate to high.      |
| 16/03/2020 | Prime Minister Johnson advises everyone against non-essential travel and contact with others. |
| 17/03/2020 | Chancellor Sunak announces that £330 billions would be made available in loan guarantees for businesses affected by the pandemic. |
| 19/03/2020 | The government introduces the Coronavirus Bill 2019–21.                           |
| 23/03/2020 | The government introduces the Coronavirus Bill 2019–21.                           |
| 24/03/2020 | G7 finance ministers and central bank governors meeting, pledging to do “whatever is necessary” to help their economies recover from the coronavirus. |
| 28/03/2020 | The Office for Budget Responsibility publishes a scenario under which UK GDP would fall by 35% in the second quarter of 2020. The International Monetary Fund estimates global GPD to decline of about 3%. |

selected equity indices (left panel) and 1-Year bond yields (right panel). The corresponding Omori power-law exponents, along with their confidence interval, are reported in the legend.

The Omori exponents are instrumental to evaluate how markets react to SARS-CoV-2 related announcements. Results show heterogeneity in the values of the Omori exponents. In the equity market, Italian and Spanish indices exhibit large exponent values, if compared to the other countries in the sample. In other words, SARS-CoV-2 related news induced sudden volatility jumps in these markets, rapidly absorbed in the after-shock time-span. This dynamics is arguably due to the fact that these countries were among the first ones affected by the spread of the disease, which fostered the sensitivity of their respective financial indices. The Omori exponents related to the CAC index, instead, suggest that SARS-CoV-2 news produce high volatility jump on the French financial market, which are slowly re-absorbed during the post-shock phase. Evidences also suggest that volatility outbursts related to the UK equity index are built up more slowly than the other markets before the shock, whereas the US equity index exhibits a slower volatility relaxation dynamics than other countries firstly affected by the virus.

The bond yield series show Omori exponents that are more heterogeneously distributed across countries. Indeed, we observe that the pre-shock exponents are relatively high in Spain and, partially, in France if compared with the after-shock exponents, meaning that bond markets seem to exhibit sudden volatility jumps just prior the occurrence of news, which are then slowly reabsorbed by market dynamics. In other cases, a similar behaviour emerges only for the pre-shock phase, such as for the UK bond index. Interestingly, we also find negative aftershock exponents, although statistically significant only for Italy and Germany in the aftershock, which can be interpreted as a dominance of aftershocks further away from mainshocks over the volatility cascade around the main event date. More in general, bond yields show lower Omori exponents than those observed for equity indices, thus suggesting that the bond market incorporate less efficiently SARS-CoV-2 related shocks.

In the lower panels of Fig. 5 we illustrate the empirical CDF of the two Omori exponents $\beta_{Aft}$ and $\beta_{Pre}$ – computed by pooling the entire set of SARS-CoV-2 news. The after-shock empirical CDF of $\beta_{N}$ for the equity indices shows larger values if compared to the pre-shock distribution. Thus, higher values of $\beta_{Aft}$ with respect to $\beta_{Pre}$ indicate that the response time after the news date $T_{i}$ is generally shorter than the activation time leading to it. When considering bond yields, instead,
Fig. 2. Volatility patterns for selected equity indices and bond yields along with the events dates. Column bars represent, for each country, the daily volatility of the reference index (upper panel) and the daily volatility of the reference bond yields (lower panel). The dashed black lines identify the dates of the relevant events, which mainly impacted the course of the national equity and bond markets.

Fig. 3. Volatility correlations across equity indices and bond yields. The figure shows the pairwise Pearson correlation coefficients among the volatility series of the considered financial indices (left panel) and bond yields (right panel). Darker colours correspond to higher correlated pairs.

the difference between $\beta^{af}$ and $\beta^{pr}$ is less prominent. This suggests that volatility in the bond markets induced by SARS-CoV-2 announcements is more persistent than that of equity markets, which instead reacts more timely to such exogenous shocks. This empirical outcome is in line with the studies on cross-market financial shock transmission, which find that the volatility shocks in the equity market are absorbed much more quickly than those in the bond one — see, for instance, [54].

Finally, we study the relationship between the size of the largest shock $V_1 = V(T_c)$ and the second largest shock $V_2$, before and after $T_c$ by means of the Bath law. Fig. 6 reports a scatter plot of $V_1$ and $V_2$, where $qft$ stands for aftershock,
Volatility distributions of equity indices and bond yields. The figure reports the volatility distributions for the reference financial indices (left panels) and bond yields (right panels). Red dashed lines the 85-th percentiles taken as reference for identifying high volatility movements.

Average distribution of large volatility occurrences and Omori exponents. The upper panels report the log-log plot of the average cumulative distribution of large volatility movements around the days of SARS-CoV-2 related announcements. The legend provides the values of the Omori exponents for both pre-shocks and after-shocks. The lower panels show the cumulative distributions of the pooled pre-shock and after-shock Omori exponents. In particular, the red colour is used to identify the empirical CDF of the pre-shock exponents, while the blue colour is associated with the after-shock distribution. Results are presented both for the selected equity indices (left panel) and bond yields (right panel).

for the equity market, which shows a linear relation corresponding to \( B_{\text{Aft}} = 0.023 \) while for the pre-shock case (indicated by \( \text{pre} \)) we have \( B_{\text{pre}} = 0.16 \). Similarly, for the bond market (see Fig. 7) we find about \( B_{\text{Aft}} = 0.199 \) for the after-shock case and for the pre-shock case we report \( B_{\text{pre}} = 0.089 \).

On the one hand, comparing the values of \( B_{\text{pre}} \) and \( B_{\text{Aft}} \), evidence supports the fact that the magnitude of pre-shocks preceding a volatility mainshock in the stock markets is generally larger than that of the aftershocks which immediately follow it. On the other hand, the size of volatility aftershocks which follow a mainshock is generally greater than that related to pre-shocks in the bond market. This provides further evidence on the fact that the effects of SARS-CoV-2 news shocks are more persistent in the credit market rather than in the stock market.

4. Concluding remarks

The spread of the novel SARS-CoV-2 has posed unprecedented economic and financial challenges for all the world countries, bearing a striking geo-economic shock to their financial markets. Economists such as [55] and [56] relate
Fig. 6. The relationship between the size of the main shock $V(T_c)$ and the size of the second largest aftershock (or pre-shock) $V_2$ for the stock market. As with the Bath law for earthquakes, we observe a proportional relation $V_2 = C B V(T_c)$ which corresponds to a Bath parameter $B = -\log_{10} C_B$. For the after-shock case we have $B_{Aft} = 0.023$ and for the pre-shock case we report $B_{Pre} = 0.16$.

Fig. 7. The relationship between the size of the main shock $V(T_c)$ and the size of the second largest aftershock (or pre-shock) $V_2$ for the bond market. As with the Bath law for earthquakes, we observe a proportional relation $V_2 = C_B V(T_c)$ which corresponds to a Bath parameter $B = -\log_{10} C_B$. For the after-shock case we have $B_{Aft} = 0.088$ and for the pre-shock case we report $B_{Pre} = 0.199$.

the current pandemic outbreak to a natural disaster rather than to an economic recession. Indeed, such an exogenous event has hit the markets in the same way as an earthquake, inducing foreshock and aftershock volatility spikes in financial markets worldwide around the neighbourhood of SARS-CoV-2 major events. In line with cascade effects of energy propagation which occur after earthquakes, we have proposed to investigate whether SARS-CoV-2 related news produce dynamic relaxation in the financial volatility of major equity indices and government bond yields.

Our empirical investigation provides evidence on the fact that: (i) financial markets heterogeneously react to news related to the pandemics, depending on their reference country, and on their foreshock and aftershock behaviour; (ii) financial markets firstly impacted by the epidemics tend to discount news effects earlier, although the impact of shocks on the Italian and German bond markets are deferred with respect to the actual date of announcement; (iii) bond market foreshocks and aftershocks are almost symmetric in their dynamics, whereas for equity markets the aftershock relaxation dynamics is faster than the foreshock volatility outburst; (iv) the sovereign bond market is generally less efficient than
the equity market at incorporating volatility shocks, meaning that volatility shocks induced by SARS-CoV-2 related events are more persistent in the credit market.

CRediT authorship contribution statement

Paolo Pagnottoni: Data curation, Writing – original draft, Conceptualization, Methodology, Writing – reviewing & editing. Alessandro Spelta: Conceptualization, Methodology, Software, Writing – original draft. Nicolò Pecora: Visualization, Investigation, Writing – original draft. Andrea Flori: Writing - original draft, Writing – reviewing & editing. Fabio Pammi: Writing – reviewing & editing.

Declaration of competing interest

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

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