The energy cascade from warm dark matter decays

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ABSTRACT

We use a set of Monte Carlo simulations to follow the cascade produced by a primary electron of energy \( E_{\text{in}} \) in the intergalactic medium. We choose \( E_{\text{in}} = 3-10 \text{ keV} \) as expected from the decay of one of the most popular warm dark matter (WDM) candidates, sterile neutrinos. Our simulation takes into account processes previously neglected such as free–free interactions with ions and recombinations, and uses the best available cross-sections for collisional ionizations and excitations with H and He and for electron–electron collisions. We precisely derive the fraction of the primary electron energy that heats the gas, ionizes atoms and produces line and continuum photons as a function of the ionization fraction. Handy fitting formulae for all the above energy depositions are provided. By keeping track of the individual photons, we can distinguish between photons in the Ly\( \alpha \) resonance and those with energy \( E < 10.2 \text{ eV} \) that do not interact further with gas. This separation is important because a Ly\( \alpha \) background can heat or cool the gas depending on the nature of the photons, and can have effects on the 21-cm radiation emitted by neutral H, which will probably become detectable at \( z > 6 \) in the near future by the next generation radio interferometers.

Key words: intergalactic medium – cosmology: theory – dark matter – diffuse radiation.

1 INTRODUCTION

The determination of the gas temperature and ionized fraction in the intergalactic medium (IGM) and interstellar medium (ISM) is fundamental for a number of astrophysical studies. In particular, it is essential for the investigation of the nearly uniform, dark, neutral state of the Universe known as Dark Ages, which has become one of the most studied topics in cosmology in the last decade. The cosmic phase between hydrogen recombination at \( z \sim 1000 \) and the so-called Epoch of Reionization (EoR) at \( z \sim 9 \) can be directly detected by the 21-cm hyperfine triplet-singlet level transition of the ground state of neutral hydrogen. A new generation of low-frequency radio interferometers such as the LOw Frequency ARray (LOFAR), the 21 Centimeter Array (21CMA), the Mileura Wide-field Array (MWA) and the Square Kilometer Array (SKA), is expected to reach the sensitivity required to map the HI distribution at angular resolution of the order of a few arcmin (e.g. Kassim et al. 2004; Pen, Wu & Peterson 2005; Wyithe, Loeb & Barnes 2005; Bowman, Morales & Hewitt 2006). If a few issues such as foreground removal, interferences from human-generated signals and ionospheric corrections will be successfully taken care of these large radio arrays will be able to perform a tomography of the Universe before and during the EoR.

It is therefore crucial to be able to predict the magnitude of the signal. The standard scenario predicts the gas temperature, \( T_K \), to decouple from the cosmic microwave background (CMB) temperature, \( T_{\text{CMB}} \), at \( z \sim 300 \). \( T_K \) then starts decreasing adiabatically until the first sources of light heat again the gas above \( T_{\text{CMB}} \) at \( z \sim 20 \). In this case, the 21-cm radiation would be seen in absorption against the CMB in the redshift interval \( 20 < z < 300 \) as discussed in detail by many recent studies (e.g. Loeb & Zaldarriaga 2004).

A number of more complex theoretical scenarios have been investigated recently. In particular, if there was a mechanism to heat the gas at \( z \geq 10 \), thus producing a thermal history different from the standard one, a direct imprint would be left on the 21-cm radiation from the neutral gas, which could then be observable in emission rather than in absorption.

First stars (Ciardi & Salvaterra 2007), intermediate-mass black holes (Zaroubi et al. 2006; Ripamonti, private communication) and decaying or annihilating warm and cold dark matter (CDM) particles (Furlanetto, Oh & Pierpaoli 2006; Shchekinov & Vasiliev 2007; Valdés et al. 2007) could be capable of leaving a significant trace in the evolution of the neutral intergalactic gas. Future 21-cm observation will possibly rule out or confirm these theoretical predictions, opening a new exciting frontier in cosmology and possibly unveiling the nature of dark matter particles.

All the most popular dark matter particle candidates inject energy into the IGM, either via decays or annihilations, initiating an energy cascade from energetic primary photons or electrons. The energy deposition depends on the large number of interactions taking place during the propagation of the cascade particles through the IGM. It is therefore very important for achieving correct results to follow in detail these cascades and to know exactly how much of the energy injected ionizes the gas, produces radiation by collisional excitations and heats surrounding medium, respectively.

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This fundamental problem has received attention in the past (e.g. Bergeron & Collin-Souffrin 1973), and the results achieved were corrected by an extensive study by Shull & van Steenberg (1985), which we will denote hereafter as SVS85, which was a development of a previous work by Shull (1979), hereafter S79.

In this work, we present the results of a Monte Carlo calculation in the spirit of the one from S79 and SVS85; in comparison, we use more recent and accurate cross-sections for collisional ionization and excitations from electron impacts, for electron–electron collisions, free–free interactions and recombinations. In addition to this, we follow in detail the radiation produced by the excitations and we are able to predict precisely how much of the energy goes into photons that do not further interact with the gas (E ≤ 10.2 eV) and how much of it contributes to the Lyα background, which directly affects the physics of the 21-cm line radiation by the so-called Wouthuysen–Field effect (e.g. Wouthuysen 1952; Field 1959; Hirata 2006) and which can heat or cool the gas depending on the nature of the Lyα photons (Chen & Miralda-Escudé 2004; Chuzhoy & Shapiro 2007).

2 METHOD

2.1 Description of the calculation

We calculate the effects produced by an X-photon of ∼keV energy injected into the IGM with T ≤ 10^4 K. At these energies, the dominant interaction is photoionization (see e.g. Zdziarski & Svensson 1989) and the X-photon ionizes an H or He atom producing an energetic primary electron. We follow the subsequent secondary cascade products.

For our calculations, we choose two specific energies for the primary electron, E_{in} = 3 and 10 keV. This energy range is of great interest because sterile neutrinos, one of the most promising WDM candidates (Dodelson & Widrow 1994; Dolgov & Hansen 2002), are expected to emit line radiation at an energy between 3 and 10 keV. A large effort has been done recently by several authors to constrain the mass and lifetime of radiatively decaying sterile neutrinos from X-ray observations (Abazajian, Fuller & Tucker 2001; Mapelli & Ferrara 2005; Abazajian 2006; Abazajian & Koushiappas 2006; Boyarsky et al. 2006a,b; Watson et al. 2006).

Once the primary electron is injected into the IGM the code calculates the cross-sections relative to a list of possible processes: H, He, He i ionization; H, He excitation; collisions with thermal electrons; free–free interactions of electrons with ionized atoms. This effects the electron would actually thermalize with the gas and as a consequence the precise heating should be calculated by taking into account the gas temperature. If the temperature is of the order of 10^4 K electrons with energies lower than 1 eV could even cool the gas.

Collisional excitations of H and He produce photons that escape freely in the surrounding medium if their energy is lower than 10.2 eV or that can further interact with the gas if they have higher energy.

The study from S79 and SVS85 derives the amount of energy which is deposited in excitation but does not give details about the individual photons. We want to estimate instead the amount of energy that goes into Lyα photons: this radiation can in fact interact further with the gas by the Wouthuysen–Field effect and is crucial to correctly estimate the 21-cm signal. Furthermore, Lyα photons by scattering resonantly off neutral hydrogen can cool or heat the gas, depending on whether they enter the resonance from its red or blue wing, respectively, as we will explain more in detail later in this Letter.

An additional novel feature of our model is the inclusion of the previously neglected two-photon forbidden transition 2s → 1s. We included both the direct collisional excitation cross-section to the 2s level and the probability that a collisional excitation to a level n ≥ 3 results in a cascade through the 2s level rather than through 2p. As noted recently (Hirata 2005; Chuzhoy & Shapiro 2007), this effect is not negligible, in general, and constitutes the most probable decay channel for H atoms excited to a level n ≥ 3 or higher. The result is the emission of two photons below the Lyα energy that do not further interact with the gas.

With our code, we are therefore able to separate the Lyα radiation from the less energetic photons produced by cascade from the 2s level. All Lyα photons that result from collisional excitations (or injected Lyα photons, see Chen & Miralda-Escudé 2004) have a cooling effect on the gas.

We also included in our calculation processes that can produce continuum photons, such as recombinations and bremsstrahlung free–free interactions of electrons with ionized atoms. These effects are negligible as we will see and there is virtually no production of photons between the Lyα and the Lyβ resonances. This radiation would have redshifted into continuum Lyα photons (Chen & Miralda-Escudé 2004) and by entering the Lyα resonance from its blue wing would have heated the gas instead.

Electron–electron collisions between secondary and thermal electrons were implemented as in SVS85 and S79, and we treated similarly the energy distribution of secondary electrons following collisional ionization of H and He, so we refer the reader to those works for a detailed explanation.

As we mentioned earlier, we found that 1000 Monte Carlo realizations gave consistent results. Going from 50 to 1000 realizations changed the averaged values by less than 5 per cent and the respective σ by less than 10 per cent. We deemed 1000 to be a sufficient number of realizations for a stable result. The 1σ values of the energy deposition fractions are included in Table 1 and they vary from 2.9 to 0.04 per cent of the total amount of energy.

2.2 Cross-sections

For our purposes, it is important to use the best available cross-sections for the several interaction channels considered in our calculation. We will give here the references rather than entering in the description of physical details that are not the scope of this Letter.
The cross-sections (σ) for collisional ionization of H, He, He⁺ were taken from Kim & Rudd (1994), Shah, Elliot & Gilbody (1987) and Shah et al. (1988). A simple functional fit is

\[ \sigma(x) = \frac{4 \pi a_0^2}{x} \left[ a \ln(x) + b \left( 1 - \frac{1}{x} \right) + c \ln(x+1) \right], \]

where \( x = E_{\text{ion}}/E_B \) is the ratio between the incoming electron energy and the binding energy of the atomic electron.

The collisional excitation cross-sections of H and He are from Stone, Kim & Desclaux (2002), while for the excitation to the 2s level of H we used the work from Bransden & Noble (1976). The cross-section for Coulomb collisions between electrons is from Spitzer & Scott (1969) as in S79, while the free–free cross-section (σ_{ff}) for electrons interacting with protons is given by the Bethe–Heitler quantum-mechanical Born approximated result (see e.g. Haug 1997),

\[ \frac{d\sigma_{ff}}{dk} \approx \frac{16\alpha Z^2r_0^2}{3k^3p^2} \ln \left( \frac{p_1 + p_2}{p_1 - p_2} \right), \]

where \( m_e \) is the electron mass, \( r_0 \) is the classical electron radius, \( \alpha \) is the fine structure constant, \( k = E/mc^2 \) is the photon energy in units of \( mc^2 \), and \( p_i, p_f \) are the momenta of the incident and scattered electron, respectively, again in units of \( mc^2 \).

As mentioned before, we also included the recombination cross-section \( \sigma_r \), to take into account a process which could produce continuum photons. Neglecting helium recombinations, we have that for hydrogen:

\[ \sigma_r(v, n) \approx 3 \times 10^{16} \frac{8n}{v_n^2v_e^2} \text{ cm}^2, \]

where \( 8n \) is the Gaunt factor of \( \mathcal{O}(1) \), \( v \) is the emitted radiation frequency, \( v_e \) is the electron velocity and \( n \) is the level at which the electron recombines.

### 3 RESULTS

Our results are summarized in Table 1 and in Fig. 1. In the table, we report the fraction of the energy of a 10 keV primary electron which, for different values of the gas-ionized fraction \( x_e \), is deposited into heat, Lyα excitations, ionizations and photons with \( E < 10.2 \text{ eV} \). The errors correspond the standard deviation from the mean calculated over 1000 Monte Carlo realizations of the experiment.

The energy fraction that goes into heating grows rapidly as the gas ionization fraction value becomes higher. The physical reason of this
behaviour is that electron–electron interactions become dominant for high values of $x_e$.

We performed our calculations for 3 and 10 keV to account for the theoretically and observationally inferred range of the sterile neutrino mass and found that the energy fraction distributed among the different processes remains similar in both cases (within 2 per cent). This is in agreement with the results from S79 and SVS85 that find that for primary electrons with energies higher than 100 eV, the fractional energy depositions converge rapidly to a common behaviour.

We gave a convenient functional form to our results by fitting the data in Table 1 with an accuracy greater than 3.5 per cent.

(i) Fraction $f_h$ of the primary energy deposited into heat:

$$f_h = 1.0 - 0.8751 \left( 1.0 - x_e^{0.4053} \right).$$

(ii) Fraction $f_a$ of the primary energy converted into Lyα radiation:

$$f_a = 0.3484 \left( 1.0 - x_e^{0.3065} \right)^{0.9533}.$$  

(iii) Fraction $f_i$ of the primary energy deposited into ionizations:

$$f_i = 0.3846 \left( 1.0 - x_e^{0.5207} \right)^{1.1952}.$$  

(iv) Fraction $f_c$ of the primary energy deposited into continuum radiation:

$$f_c = 0.1537 \left( 1.0 - x_e^{0.3224} \right).$$

Our results differ sensibly from those of the past studies, with differences as high as 30 per cent for some values of $x_e$. The reason for this is a combination of the better and more modern cross-sections which we used and of the additional processes included in the calculation such as the transitions through the 2s level of H. We compare in detail our results with those obtained by SVS85 in Fig. 2. While for small values of $x_e$, the curves are similar it is evident that the differences become substantial for $x_e \gtrsim 0.1$.

4 DISCUSSION AND CONCLUSIONS

We have presented an updated calculation of the energy cascade arising from a primary electron with energy in the range (3–10 keV) predicted for one of the most popular dark matter particle candidates, i.e. sterile neutrinos. We have computed the fractional energy deposition into ionizations, excitations and heating to a new level of detail and followed the fate of individual photons to be able to distinguish between Lyα injected radiation and continuum photons with energies under 10.2 eV.

As mentioned previously in this work, Lyα radiation affects the gas in several ways. It has a thermal effect on the matter, with a heating or a cooling effect depending on the nature of the photons. Line or injected Lyα photons cool the gas, while photons between the Lyα and Lyβ resonances that redshift to 10.2 eV (continuum Lyα photons) act as a heat source for the gas.

A Lyα background is also responsible for the Wouthuysen–Field process, which directly affects the physics of the 21-cm line radiation from neutral H and can make it visible in emission or absorption against the CMB. This aspect is important because 21 cm observations of the high-redshift Universe will be performed in the near future by next generation low-frequency radio interferometers such as LOFAR.

We included in our calculations the only mechanisms that could produce continuum Lyα radiation, recombinations and free–free interactions with ions. Both processes are more probable as the ionized fraction increases, but at the same time the cross-section for electron–electron collisions becomes dominant, so we found that both these channels are practically negligible and also found that electrons injected in a highly ionized gas are thermalized before they can produce continuum photons.

We expect that the same calculations performed for relativistic electrons could produce interesting results in this sense, also taking into account that processes such as inverse-Compton on CMB photons would become important and produce continuum radiation. This could be a useful extension to this work and could be applied to study the effects of light dark matter decays/annihilations in the energy range around ~10 MeV.

REFERENCES

Abazajian K., 2006, Phys. Rev. D, 73f, 3506
Abazajian K., Koushiappas S. M., 2006, Phys. Rev. D, 74, 023527
Abazajian K., Fuller G. M., Tucker W. H., 2001, ApJ, 562, 593
Bergeron J., Collin-Souffrin S., 1973, A&A, 25, 1
Bowman J., Morales M., Hewitt J., 2006, ApJ, 638, 20
Boyarsky A., Neronov A., Ruchayskiy O., Shaposhnikov M., 2006a, MNRAS, 370, 213
Boyarsky A., Neronov A., Ruchayskiy O., Shaposhnikov M., 2006b, Phys. Rev. D, 74, 103506
Bransden B. H., Noble C. J., 1976, J. Phys. B, 9, 1507
Chen X., Miralda-Escude J., 2004, ApJ, 602, 1
Chuzhoy L., Shapiro P. R., 2007, ApJ, 655, 843C
Ciardi B., Salvaterra R., 2007, MNRAS, 381, 1137
Dodelson S., 2008, MNRAS, 387, 213
Dolgov A. D., Hansen S. H., 2002, Astropart. Phys., 16, 339
Dolgov A. D., Hansen S. H., 2002, Astropart. Phys., 16, 339
Field G. B., 1959, ApJ, 129, 551
Furlanetto S. R., Oh S. P., Pierpaoli E., 2006, Phys. Rev. D, 74j, 3502
Haug E., 1997, A&A, 326, 417
Hirata C. M., 2006, MNRAS, 367, 259
Kassim N. E., Lazio T. J. W., Ray P. S., Crane P. C., Hicks B. C., Stewart K. P., Cohen A. S., Lane W. M., 2004, Planet. Space Sci., 52, 1343
Kim Y.-K., Rudd M. E., 1994, Phys. Rev. A, 50, 3954
Loeb A., Zaldarriaga M., 2004, Phys. Rev. Lett., 92, 211301
Mapelli M., Ferrara A., 2005, MNRAS, 364, 2
Peterson J. B., Pen U. L., Wu X. P., 2005, in Kassim N. E., Perez M. R., Junor W., Henning P. A., eds, ASP Conf. Ser. Vol. 345, Searching for Early Ionization with the Primeval Structure Telescope. Astron. Soc. Pac., San Francisco, p. 441

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Valdés M., Ferrara A., Mapelli M., Ripamonti E., 2007, MNRAS, 377, 245V
Watson C. R., Beacom J. F., Yüksel H., Walker T. P., 2006, Phys. Rev. D, 74c, 3009
Wouthuysen S. A., 1952, AJ, 57, 31
Wyithe J. S., Loeb A., Barnes D., 2005, ApJ, 634, 715
Zdziarski A. A., Svensson R., 1989, ApJ, 344, 551
Zaroubi S., Thomas R. M., Sugiyama N., Silk J., 2006, MNRAS, 375, 1269

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