LETTER TO THE EDITOR

Cold CO in circumstellar disks
On the effects of photodesorption and vertical mixing

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ABSTRACT

\textbf{Aims.} We attempt to understand the presence of gas phase CO below its sublimation temperature in circumstellar disks. We study two promising mechanisms to explain this phenomenon: turbulent mixing and photodesorption.

\textbf{Methods.} We compute the chemical evolution of circumstellar disks including grain surface reactions with and without turbulent mixing and CO photodesorption.

\textbf{Results.} We show that photodesorption significantly enhances the gas phase CO abundance, by extracting CO from the grains when the visual extinction remains below about 5 magnitudes. However, the resulting dependence of column density on radial distance is inconsistent with observations so far. We propose that this inconsistency could be the result of grain growth. On the other hand, the influence of turbulent mixing is not found to be straightforward. The efficiency of turbulent mixing depends upon a variety of parameters, including the disk structure. For the set of parameters we chose, turbulent mixing is not found to have any significant influence on the CO column density.

\textbf{Key words.} Stars: circumstellar matter - Planetary systems: protoplanetary disks - Astrochemistry - Turbulence

1. Introduction

In circumstellar disks, because of the high densities, carbon monoxide is expected to stick onto grains at temperatures below about 17 K. However, millimeter interferometric observations of several circumstellar disks around T Tauri stars (e.g. DM Tau, GM Aur, and LkCa15) have revealed that a large amount of CO remains gaseous at temperatures as low as 10 K (Dartois et al. 2003; Piétu et al. 2007). These authors show that the bulk of CO is at temperatures below 17 K between 100 and 800 AU from the central star. Since these disks are much older than the sticking timescale of CO onto grains (∼ 10^7 yr), some mechanism must prevent the complete depletion of CO.

Aikawa & Nomura (2006) proposed that the presence of cold CO in disks can be a consequence of vertical turbulent mixing (See also Fig. 4 of Willacy et al. 2006). Semenov et al. (2006) studied in detail the influence of both vertical and radial mixing on the abundance of cold CO. They found that vertical mixing cannot account for the observed abundance of cold CO, while the situation improves slightly when considering the full 2D mixing (vertical and radial). However, Aikawa (2007) computed analytically the influence of vertical mixing on the abundance of cold CO and concluded that vertical mixing was sufficient to achieve an abundance of CO consistent with that observed by Dartois et al. (2003). The apparent discrepancy with Semenov et al. (2006) can be understood as a consequence of the different efficiencies of grain surface reactions in their studies (Aikawa 2007).

On the other hand, Oberg et al. (2007) measured the photodesorption rate of CO in the laboratory. They found a rate similar to that found for H$_2$O by Westley et al. (1995), about 2 orders of magnitude higher than previously available theoretical estimates (Draine & Salpeter 1979), implying that this non-thermal desorption process was an appealing candidate for explaining the abundance of cold CO in various astrophysical environments. This motivated us to investigate the influence of both vertical mixing and photodesorption on the CO column density in disks, using a parametric model consistent with interferometric observations of circumstellar disks.

In Sect. 2, we describe the physical and chemical model used, while Sect. 3 is devoted to the results of our computations. In Sects. 4 and 5 we discuss our results and present our conclusions.

2. Modeling

2.1. Disk structure

To consistently compare with the physical structure observed by Piétu et al. (2007), we use a simple disk model with physical quantities varying as power laws of the radius, similar to the parametric disk model used by Piétu et al. (2007) to reproduce their interferometric maps. The vertical temperature distribution is defined to have two layers, one cold layer with a constant temperature of 10 K, and a warm layer in radiative equilibrium with the central star radiation. This behavior is typical of disk models (e.g. D’Alessio et al. 1999, Aikawa & Nomura 2006). The precise location of the transition between the two layers varies between models. We chose this transition at 2 pressure scale...
heights, a location similar to that used by Dartois et al. (2003) to fit their data. The constant mid-plane temperature, although surprising at first sight, is consistent both with the temperature observed in $^{13}$CO J=1-0 by Piétu et al. (2007) and the surface density power exponent of $-3/2$ observed in the outer parts of most “undisturbed” disks (see Dutrey, 2008, for a review). In an $\alpha$-model (Shakura & Syunyaev 1973), the product of the temperature and the surface density is indeed assumed to vary as $R^{-3/2}$. Therefore, a constant mid-plane temperature in an stationary model is the only way that the surface density decreases as $R^{-3/2}$. This regions of almost constant temperature are also found in the more complete disk models developed by D'Alessio et al. (1999, 2001).

The laws that we use in the present paper are:

$$T(R,z) = T_C + (T_H(R) - T_C) \times \frac{1}{2} \left( 1 + \tanh \left( \frac{z - 2H(R)}{H(R)/3} \right) \right)$$

(1)

$$T_C = 10 \text{ K}$$

(2)

$$T_H(R) = 30 \left( \frac{R}{100 \text{ AU}} \right)^{-1/2} \text{ K}$$

(3)

$$H(R) = \frac{c_s(T_C)}{\Omega} \approx 8.4 \left( \frac{T_C}{10 \text{ K}} \right)^{1/2} \left( \frac{R}{100 \text{ AU}} \right)^{3/2} \text{ AU}$$

(4)

$$\Sigma(R) = 0.8 \left( \frac{R}{100 \text{ AU}} \right)^{-3/2} \text{ g cm}^{-2}$$

(5)

where $c_s$ is the isothermal sound speed, $\Omega$ is the Keplerian frequency, and $\Sigma$ is the surface density. From these laws, the mass density $\rho$ is then computed from the hydrostatic equilibrium.

### 2.2. Chemistry

The chemical evolution of the disk is computed with a 1D vertical model that takes into account both gas-phase and grain surface chemistries. This code was adapted from the OSU gas-grain code developed by the astrochemistry team of Eric Herbst. The formalism of surface chemistry and various processes are described in Hasegawa et al. (1992) and Garrod et al. (2007). The gas-phase chemical network uses updates from Hasegawa et al. (1992) and Garrod et al. (2007). The complete network (gas and grain) contains 655 species and 6067 reactions. Grains are assumed to be of interstellar type.

To model the CO and H$_2$ UV self-shielding, we use the approximation from Lee et al. (1996). The code is written in Fortran 90 and uses the DLSODES routine from the ODEPACK package (Hindmarsh 1983) to solve the differential equations. The initial abundances of our calculations are taken from the output of a gas-phase calculation of a dark cloud ($n_H=2 \times 10^4$ cm$^{-3}$, $T=10$ K, $A_V=10$) after 10$^7$ yr and our elemental abundances are the EA3 conditions from Wakelam & Herbst (2008), with an S abundance of $8 \times 10^{-8}$. The gas-grain model is then allowed to evolve for 10$^8$ yr with 32 vertical points. A period of 10$^8$ yr is the radial mixing timescale at 100 AU, as well as the evolutionary timescale for the disk structure. Computing for a longer time would in principle require a full 2D (R,z) approach and an evolving disk model.

### 2.3. Photodesorption

In their experiments, Oberg et al. (2007) found a photodesorption rate $Y_{PD}$ of $3 \times 10^{-3}$ CO molecules per UV photon above pure CO ice. In circumstellar disks, UV photons originate from two main processes: (i) the ambient UV field, coming from both the central star and the surrounding ISM, and (ii) secondary photons generated by the interaction of H$_2$ with cosmic rays and cosmic-ray-induced (CR) secondary electrons (Prasad & Tarafdar 1983; Shen et al. 2004). Photodesorption of CO (we did not consider photodesorption for other species) by these two sources of UV photons can be expressed by the chemical reactions:

adsorbed CO $\xrightarrow{K_{UV}}$ CO, \hspace{1cm} (6)

adsorbed CO $\xrightarrow{K_{CR}}$ CO, \hspace{1cm} (7)

where $K_{UV}$ and $K_{CR}$ are the first-order rate coefficients (s$^{-1}$). From Oberg et al. (2007) and the additional approximation that adsorbed CO molecules can always escape independently of the thickness of the adsorbed layer, we can express these rate coefficients as:

$$K_{UV} = \frac{Y_{PD}}{\Sigma_{surf}} I_{\text{ISM-FUV}} f_{UV} e^{-\gamma A_v}$$

(8)

$$K_{CR} = \frac{Y_{PD}}{\Sigma_{surf}} I_{\text{CR-FUV}}$$

(9)

(Hassel et al. in preparation) where $I_{\text{ISM-FUV}} \approx 10^8$ photons cm$^{-2}$ s$^{-1}$ is the ambient far UV field strength for a standard ISM irradiation field (Draine 1978), $I_{\text{CR-FUV}} \approx 10^8$ photons cm$^{-2}$ s$^{-1}$ is the strength of the far UV field generated by the cosmic rays, $\gamma$ measures the difference between the UV extinction and the visual extinction ($\gamma \approx 2$ for interstellar grains, Roberge et al. 1991), and $\Sigma_{surf}$ is the site density per grain surface unit (i.e. the maximum number of molecules adsorbed as a single layer on a grain per cm$^2$). The quantity $f_{UV}$ is a scale factor used to express the strength of the ambient UV field (originating mainly in the central star) as a multiple of the standard ISM radiation field. This expression is justified by noting that the UV spectrum coming from the UV excess of young stars has a similar shape to that of the standard interstellar field (Chapillon et al. 2008). In the present report, we use:

$$f_{UV} = 300 \left( \frac{\sqrt{R^2 + (4H)^2}}{100 \text{ AU}} \right)^{-2}$$

(10)

The UV field intensity is consistent with the results of Bergin et al. (2003). We consider here only the vertical extinction of the UV field. This approximation is motivated by the fact that the direct (radial) extinction of stellar UV radiation is very efficient so that most photons seen by the disk are in fact scattered by small grains at high altitudes. We consider here that this scattering acts at the edge of our computation box (4 pressure scale heights). With this law for $f_{UV}$, direct photodesorption is dominant for $A_v \lesssim 7$, while photodesorption by CR-induced UV photons (independent of $A_v$) maintains a low desorption rate in denser regions.

### 2.4. Turbulent mixing

We compute the vertical turbulent mixing using an $\alpha$ turbulent viscosity (Shakura & Syunyaev 1973), where the diffusivity $D_t$ is given by:

$$D_t = \alpha \Sigma c_s^2 \frac{H}{\Omega}$$

(11)

The Schmidt number $Sc$, defined as the ratio of the turbulent viscosity to the turbulent diffusivity, is a poorly constrained parameter. In the present work, we set its value to be 1 and choose $\alpha = 10^{-2}$, values commonly used (e.g. Semenov et al. 2006; Willacy et al. 2006; Aikawa 2007).

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1. http://www.physics.ohio-state.edu/~eric/research.html
The resulting equations for the chemical abundances $x_i$ are:

$$\frac{\partial x_i}{\partial t} = P_i - L_i + \frac{1}{\rho} \frac{\partial}{\partial z} (D \frac{\partial}{\partial z} x_i)$$

where $P_i$ and $L_i$ are the chemical production and loss terms.

The vertical mixing and the chemistry are computed using first-order operator splitting, the chemistry being computed before the mixing inside a time step. This induces intrinsic errors, which are controlled by reducing the time step. We adapted the time step so that the splitting errors remain below 5% relative accuracy, by comparing with simulations without operator splitting, which are far more time-consuming.

3. Results

The vertical distribution of gas phase CO was computed at 100, 200, 300, 400, 500, and 600 AU, for 4 different models, with or without CO photodesorption and/or vertical mixing. Figures 1, 2, and 3 show the resulting vertical CO distributions. The “handle-bar” shape of the vertical abundance profile at all radii is the result of CO photodissociation at high altitudes (mostly visible at 300 and 500 AU) and CO freezing onto grains in the dense mid-plane (below $z/H \cong 2$). Carbon is locked in different dominant forms as a function of height: frozen CO in the mid-plane, then frozen CO$_2$, gaseous CO, and finally atomic C in the photodissociated region. The thickness of each layer depends on the radius (through density, temperature, and Av). In the 100 AU profile (Fig. 1), a dip is visible in the CO distribution without mixing. This dip is the consequence of a layer of N$_2$H$^+$, which initiates a secondary reaction chain (dominated by grain chemistry) started by:

$$\text{N}_2\text{H}^+ + \text{CO} \rightarrow \text{N}_2 + \text{HCO}^+.$$  

HCO$^+$ is then converted into other carbon-bearing molecules, the reaction chain ending with frozen CO$_2$.

The CO column density as a function of radius is displayed in Fig. 4.

3.1. Influence of photodesorption

Photodesorption by primary UV photons is the most important process affecting the abundance of gas-phase CO. When the visual extinction is sufficiently low (below about 5 mag), this desorption mechanism is efficient enough to preserve a significant abundance of CO. For radii larger than 200 AU, the total column density of gas phase CO is increased by an order of magnitude when this process is taken into account. The situation is different at 100 AU. Here, the visual extinction reaches a value of 5 mag at 2 pressure scale heights, and grains receive insufficient primary UV photons to enable efficient photodesorption of CO. The secondary UV photons originating from the interaction of H$_2$ with electrons induced by cosmic rays are then the only photodesorbing photons. They maintain a small fraction of CO in the gas phase but do not influence the total CO column density by more than 10%.

3.2. Influence of vertical mixing

In our simulations, vertical mixing has a small influence on the total column densities of CO. At 100 AU (and 200 AU), as shown in Fig. 4, the presence of a layer of N$_2$H$^+$ appears as a sink of CO (via reaction (13)) and the total CO column density is reduced by vertical mixing. This is the reason why the CO abundance below $z = 2H$ is lower in the case with diffusion (Fig. 1).
The low efficiency of vertical mixing is a consequence of two effects. First, when CO condenses onto grains, grain chemistry transforms it into more refractory species, thereby preventing desorption when it diffuses back to the warm region. The second reason is the consequence of a dilution effect. Due to a temperature transition at 2 pressure scale heights, the warm region represents less than 10\% of the total mass. This is obviously a possible bias of our disk model, the influence of vertical mixing being very sensitive to this transition. For a transition deeper inside the disk, as considered by Aikawa & Nomura (2006) and Aikawa (2007), vertical mixing is far more efficient. Accurate knowledge of the true thermal structure of the disk would be required to obtain a more precise estimate.

4. Discussion

Figure 4 shows that photodesorption increases the total CO column density, but also makes the CO column density flatter. Piétu et al. (2007) measured a steep radial profile of CO column density, varying as R^{-3} or even more steeply, with about 10^{17} cm^{-2} at 300 AU. This gradient is steeper than for our models without photodesorption. Quantitative comparisons with observations are however far from being straightforward because they require the generation of CO emission maps and iterations on the physical structure to find the best fit for each chemical setup. Incidentally, the flat CO column density profile is a common feature of disk chemical models. In our case, we would like to raise a few points:

- Our results are extremely sensitive to the location of the transition between the cold and warm regions. We chose a transition at 2 pressure scale heights; other choices would lead to significant differences in the column density radial profile.
- At large distances from the central star, the CO column density is very sensitive to photodissociation. The stellar UV flux is not constrained accurately, although its value can significantly alter our results. Our treatment of the UV field is also approximate. We only consider UV radiation in a direction perpendicular to the disk. Observations of 12CO are sensitive only to the outer regions (Piétu et al. 2007), where the interstellar UV field impinging from the disk edge will steepen the slope of the CO column density profile.
- For a given UV flux, photodissociation is controlled by the relation between visual extinction and column density. This factor depends mostly upon the amount of small grains. Grain growth can change the penetration of UV radiation inside the disk and dissociate CO further (see Chapillon et al. 2008). Since grain growth rates depend upon density, the grain distribution can depend upon the radial distance and completely change the radial profile of the CO column density. In turn, it may be possible to invert the CO column density to infer some information about the current state of grain growth at a given radius.
- Grain growth also increases the timescales for the adsorption of CO and grain surface chemical reactions, making both photodesorption and vertical mixing more efficient at retaining CO in the gas phase.

5. Conclusions

We have shown that CO photodesorption appears to be a good candidate to explain the abundance of cold gas phase CO in circumstellar disks. However, it tends to create a flatter radial profile for the CO column density, in contrast to that observed in disks. Therefore, more work is necessary to solve this problem. Consideration of the photodissociating UV flux and variations in its penetration inside the disk due to grain growth and geometry seem to provide an avenue to improve our modelling of circumstellar disks. Moreover, we have shown that the influence of vertical mixing on the abundance of CO is not straightforward. Rather, the efficiency of vertical mixing depends upon many parameters, including the details of the disk structure (density and temperature) and the level of grain growth, all of which remain uncertain today.

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