THE SUBMILLIMETER AND MILLIMETER EXCESS OF THE SMALL MAGELLANIC CLOUD: MAGNETIC DIPOLE EMISSION FROM MAGNETIC NANOPARTICLES?

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ABSTRACT

The Small Magellanic Cloud (SMC) has surprisingly strong submillimeter- and millimeter-wavelength emission that is inconsistent with standard dust models, including those with emission from spinning dust. Here, we show that the emission from the SMC may be understood if the interstellar dust mixture includes magnetic nanoparticles, emitting magnetic dipole radiation resulting from thermal fluctuations in the magnetization. The magnetic grains can be metallic iron, magnetite Fe₃O₄, or maghemite γ-Fe₂O₃. The required mass of iron is consistent with elemental abundance constraints. The magnetic dipole emission is predicted to be polarized orthogonally to the normal electric dipole radiation if the nanoparticles are inclusions in larger grains. We speculate that other low-metallicity galaxies may also have a large fraction of the interstellar Fe in magnetic materials.

Key words: dust, extinction – infrared: galaxies – infrared: ISM – Magellanic Clouds – polarization – radiation mechanisms: thermal – radio continuum: ISM

Online-only material: color figures

1. INTRODUCTION

Low-metallicity dwarf galaxies often exhibit surprisingly strong emission at submillimeter (submm) and millimeter (mm) wavelengths (e.g., Galliano et al. 2003, 2005; Galametz et al. 2009; Grossi et al. 2010; O’Halloran et al. 2010; Galametz et al. 2011), substantially exceeding what is expected based on the observed emission from dust at shorter wavelengths. This “submm excess” could in principle be due to a large mass of cold dust, but in some cases the implied dust masses are too large to be consistent with the observed gas mass and metallicity.

The Small Magellanic Cloud (SMC) is a prime example of this phenomenon. The dust spectral energy distribution (SED) has been measured from near-infrared through cm wavelengths. Israel et al. (2010), Bot et al. (2010), and Planck Collaboration et al. (2011b) concluded that conventional dust models cannot account for the observed submm–microwave emission from the SMC. Upper limits on dust masses in the SMC are obtained in Section 2. The observed SED of the SMC, and the emission attributed to dust, is reviewed in Section 3, and in Section 4 we show that models with Milky Way dust opacity cannot reproduce the observed SED. Planck Collaboration et al. (2011b) further showed that the emission shortfall could not be accounted for by spinning dust.

Large submm excesses have also been reported for other low-metallicity dwarf galaxies. NGC 1705 has received particular attention (Galametz et al. 2009; O’Halloran et al. 2010; Galametz et al. 2011) and substantial excesses have also been reported for a number of other systems, including Haro 11, II Zw 40, and NGC 7674 (Galametz et al. 2011).

This excess emission challenges our understanding of interstellar dust. If the submm excess in low-metallicity dwarfs is due to thermal emission from dust, these galaxies either contain surprisingly large masses of very cold dust, or the dust opacity at submm frequencies must substantially exceed that of the dust in normal-metallicity galaxies, such as the Milky Way.

In the Galactic interstellar medium (ISM), typically 90% or more of the Fe is missing from the gas phase (Jenkins 2009), locked up in solid grains. Thus, Fe accounts for ∼25% of the dust mass in diffuse interstellar regions, although as yet we know little about the nature of the Fe-containing material. Interstellar dust models based on amorphous silicate and carbonaceous material (e.g., Mathis et al. 1977; Draine & Lee 1984; Weingartner & Draine 2001; Zubko et al. 2004; Draine & Li 2007; Draine & Fraisse 2009) often posit that the Fe missing from the gas is incorporated in amorphous silicate material, but it is entirely possible for much or most of the solid-phase Fe to be in the form of metallic Fe or certain Fe oxides, such as magnetite, that are spontaneously magnetized.

Draine & Lazarian (1999, hereafter DL99) noted that ferromagnetic or ferrimagnetic materials can have large opacities at microwave frequencies. Draine & Hensley (2012) recently re-estimated the absorption cross sections for nanoparticles of ferromagnetic or ferrimagnetic materials. They considered three naturally occurring magnetic materials—metallic iron, magnetite, and maghemite—and found that the magnetic response implies a large opacity at submm and mm wavelengths.

Here, we propose that magnetic nanoparticles may provide the 100–500 GHz opacity needed to account for the strong submm–microwave emission from the SMC. Upper limits on dust masses in the SMC are obtained in Section 2. The observed SED of the SMC, and the emission attributed to dust, is reviewed in Section 3, and in Section 4 we show that models with Milky Way dust opacities cannot reproduce the observed SED. The contribution of spinning dust is discussed in Section 5, where we show that spinning dust cannot account for the observed emission near ∼100 GHz. In Section 6, we consider dust models for the SMC that include maghemite, magnetite, and metallic iron grains. We find that the submm and mm excess in the SMC can be accounted for by a population of magnetic nanoparticles.

In Section 7, we discuss other evidence for the formation of Fe or Fe-oxide nanoparticles, and speculate on why the dust in low-metallicity galaxies such as the SMC differs from the dust in normal-metallicity spirals, such as the Galaxy. We also discuss the predicted polarization of the emission from the SMC. Our results are summarized in Section 8.

2. MASS OF THE ISM IN THE SMC

At a distance $D = 62$ kpc (Szewczyk et al. 2009), the SMC provides an opportunity to study the dust in a low-metallicity dwarf galaxy. The present study will concentrate on the 2:38 radius ($\Omega = 0.00542 \text{sr} = 17.8 \text{ deg}^2$) region (centered on
The sightline toward $\alpha$ SMC radial velocities is 2100 Jy MHz (mean line intensity 1318 K km s$^{-1}$) studied by Planck Collaboration et al. (2011b). The 21 cm line flux from this region ranges from 0.25 to 10$^9$ M$_{\odot}$ (not including He) within the 0$^\circ$ 40 radius region. We include their extractions for the 10 COBE-DIRBE bands (1.27–248 $\mu$m) a comment on the SMC. Foreground removal was done by subtracting the mean brightness of adjacent off-source regions. Aguirre et al. (2003) also extracted 100, 140, and 240 $\mu$m fluxes for COBE-DIRBE (Silverberg et al. 1993).

Japan et al. (2010) extracted fluxes for a 2:40 radial region ($\Omega = 0.00544$ sr) centered on the SMC. We show their extractions for the 10 COBE-DIRBE bands (1.27 $\mu$m to 248 $\mu$m).

3. SED OF THE SMC

Figure 1 shows the observed global SED of the SMC, after removal of smooth foregrounds and backgrounds, from the following compilations.

Haynes et al. (1991) reported global flux densities measured with the Parkes 64 m telescope at 1.4, 2.45 GHz, 4.75, and 8.55 GHz; the 1.4 GHz flux density is a revision of the result of Loiseau et al. (1987). Mountfort et al. (1987) measured the 2.3 GHz flux density with the Hartebeesthoek 26 m telescope.

The TopHat balloon experiment (Aguirre et al. 2003) measured the flux in four bands (245–630 GHz) in a 2:40 radius region ($\Omega = 0.00544$ sr) centered on the SMC. Foreground removal was done by subtracting the mean brightness of adjacent off-source regions. Aguirre et al. (2003) also extracted 100, 140, and 240 $\mu$m fluxes for COBE-DIRBE (Silverberg et al. 1993).

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Gordon et al. (2011) extracted fluxes for a 2:25 radial region ($\Omega = 0.00484$ sr) centered on the SMC, measured using the IRAC (Fazio et al. 2004) and MIPS (Rieke et al. 2004) cameras on the Spitzer Space Telescope (Werner et al. 2004). Foreground removal consisted of subtracting the mean brightness of an annulus extending from 2:3 to 2:5.

Planck Collaboration et al. (2011b) extracted fluxes for a 2:38 radial region ($\Omega = 0.00542$ sr) centered on the SMC. Foreground subtraction consisted of subtracting the mean brightness of a 1$^\circ$ annulus around the extraction region. We include their extractions for Planck (nine bands, 30–858 GHz; Planck Collaboration et al. 2011a), WMAP (five bands, 23–94 GHz; Bennett et al. 2003), and IRAS (four bands, 12–100 $\mu$m; Miville-Deschênes & Lagache 2005).

Planck Collaboration et al. (2011b) further corrected the foreground removal by taking into consideration the difference in $\sigma$(H$^1$) at Galactic radial velocities between the background annulus and the extraction aperture.2

Figure 1(a) shows the spectrum of the 0.00542 sr region centered on the SMC. We assume that the differences in coverage ($\Omega$ ranging from 0.00484 sr to 0.00542 sr) are unimportant, as most of the flux will come from the central regions. Planck Collaboration et al. (2011b) estimate that cosmic microwave background (CMB) fluctuations add emission corresponding to a mean CMB temperature excess ($\Delta T_{\mathrm{CMB}}$) of 58 $\mu$K over the

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1. The sightline toward $\alpha$ Oph is ice-free. We assume that ices are a negligible fraction of the total dust mass in the SMC.

2. We do not show the “corrected” Planck fluxes for IRAS12 and IRAS25 because the entries for $J_{\nu}$th in Table 2 of Planck Collaboration et al. (2011b) do not appear to be correct.
estimates for $F_{\nu}$). The spectrum of this CMB excess

$$\Delta CMB = \Omega \langle \Delta T_{\text{CMB}} \rangle \left. \frac{\partial B_{\nu}}{\partial T} \right|_{T = 2.726 K}$$

is plotted in Figure 1(a).

To isolate the emission from the dust, it is necessary to subtract free–free and synchrotron emission. We find the observations to be consistent with synchrotron and free–free spectra

$$F_{\nu}^{\text{synch}} \approx 36. \left( \frac{\nu}{10 \ \text{GHz}} \right)^{-1.0} \ \text{Jy}$$

$$F_{\nu}^{\text{ff}} \approx 11.0 \frac{g_{\text{ff}}(\nu, T)}{g_{\text{ff}}(10 \ \text{GHz}, T)} e^{-h(\nu - 10 \ \text{GHz})/kT} \ \text{Jy}$$

with $T = 10^4 K$. Our estimate for $F_{\nu}^{\text{ff}}(10 \ \text{GHz})$ is intermediate between the 13.4 Jy estimate of Israel et al. (2010) and the 9.05 Jy estimate of Planck Collaboration et al. (2011b). Our estimates for $F_{\nu}^{\text{ff}}$ and $F_{\nu}^{\text{synch}}$ are shown in Figure 1(a). The Gaunt factor $g_{\text{ff}}(\nu, T)$ is obtained from Equation (10.9) of Draine (2011). For $n(\text{He}^+)/n(\text{H}^+) = 1.08$ and $T = 10^4 K$, this corresponds to $\int n_e n_i(\text{He}^+)dV = 1.45 \times 10^{46} \ \text{cm}^{-3}$ and an H photoionization rate $Q_0 = 3.7 \times 10^{51} \ \text{s}^{-1}$.

The residual after subtraction of $(\Delta CMB)_\nu$, $F_{\nu}^{\text{ff}}$, and $F_{\nu}^{\text{synch}}$ is shown in Figure 1(b). This residual is presumed to be emission from dust and (at short wavelengths) stars. A smooth curve has been drawn through the points to guide the eye. Subtracting an estimate for the starlight continuum as in Figure 1(b), the integrated $\lambda > 5 \ \mu m$ dust luminosity of the SMC is $L_d(\lambda > 5 \ \mu m) = 1.00 \times 10^9 (D/62 \ \text{kpc})^2 L_\odot$.

4. CONVENTIONAL DUST MODELS

The observed infrared and submm emission from normal-metallicity star-forming spiral galaxies appears to be consistent with physical dust models that were developed to reproduce the observed properties of dust in the diffuse ISM of the local Milky Way, including wavelength-dependent extinction and infrared emission (e.g., Weingartner & Draine 2001; Li & Draine 2001; Zubko et al. 2004; Draine & Li 2007; Draine & Fraisse 2009; Compiegne et al. 2011). The models of Draine & Li (2007, henceforth DL07) consist of amorphous silicate grains plus carbonaceous grains; the carbonaceous grains have the physical properties of graphite when large, and the properties of polycyclic aromatic hydrocarbons (PAHs) when very small. This dust model was able to reproduce the global SEDs of the galaxies in the SINGS sample (Draine et al. 2007), including 17 galaxies with $850 \ \mu m$ SCUBA photometry. More recently, the same model has been found to be consistent with both global and spatially resolved SEDs of normal-metallicity (i.e., $0.5 < Z/Z_\odot < 2$) galaxies in the KINGFISH sample (Aniano et al. 2012; G. Aniano et al. 2012, in preparation), including photometry out to 500 $\mu m$.

The DL07 dust model is able to reproduce the observed emission from dust in the diffuse ISM of the Galaxy (Finkbeiner et al. 1999) out to wavelengths as long as 2 mm (see Figure 14(a) of Draine & Li 2007). However, a significant emission excess (relative to the model) appears at $\lambda > 3 \ mm (\nu < 100 \ \text{GHz})$; this “anomalous microwave emission” (AME) has been confirmed by numerous observations (Planck Collaboration et al. 2011c and references therein). The AME in the Galaxy is thought to be mainly rotational emission from the PAH population (Draine & Lazarian 1998a, 1998b).

DL07 propose that the $3 \ \mu m < \lambda < 3 \ mm$ SEDs of entire galaxies, or large regions within a galaxy, can be fit using a dust model consisting of amorphous silicates, graphitic grains, and PAHs, and assuming that the dust heating rate is distributed according to

$$\frac{dM_d}{dU} = (1 - \gamma)M_{d,\text{tot}}(U - U_{\text{min}})$$

$$+ \gamma M_{d,\text{tot}} \frac{(\alpha - 1)U - U_{\text{min}}}{U_{\text{max}} - U_{\text{min}}} U_{\text{max}} - U_{\text{min}}$$

for $U_{\text{min}} \leq U \leq U_{\text{max}}$. 

\[ \text{(6)} \]
where $U$ is the ratio of the local dust heating rate to the heating rate produced by the solar-neighborhood starlight radiation field, $M_d(U)$ is the mass of amorphous silicate plus carbonaceous dust with heating rates $<U$, and $M_{d,\text{tot}}$ is the total dust mass. Equation (6) is a very simple distribution function, with only five parameters ($M_{d,\text{tot}}$, $U_{\text{min}}$, $U_{\text{max}}$, $\alpha$, $\gamma$), but studies of dust emission using this distribution function for the grain heating have been successful in reproducing the global emission from galaxies, as well as the emission from $\sim 500$ pc regions within galaxies (e.g., Aniano et al. 2012). The DL07 models are also characterized by the PAH abundance parameter $q_{\text{PAH}} = \frac{M_{\text{PAH}}}{M_{\text{d,\text{tot}}}}$ — the fraction of the dust mass contributed by PAH particles containing $<10^5$ C atoms.

We vary five parameters—the total dust mass $M_{d,\text{tot}}$, the PAH abundance parameter $q_{\text{PAH}}$, and the starlight heating parameters $U_{\text{min}}$, $\alpha$, and $\gamma$; $U_{\text{max}} = 10^7$ is kept fixed. Because we do not include a realistic model for the starlight contribution to the SED, the model is fit only to data at $\lambda > 3 \mu$m, where reddening by dust should be minimal. Because the emission at $\lambda > 3 \text{ mm}$ ($\nu < 100 \text{ GHz}$) may include a substantial contribution from “spinning dust,” the DL07 model + starlight is fit to $\lambda < 2 \text{ mm}$ data.

If we allow $U_{\text{min}}$ to be as low as 0.2, we obtain Model 1, shown in Figure 2. This model has a total dust mass $M_{d,\text{tot}} = 1.3 \times 10^6 M_\odot$, exceeding the upper limit of $1.1 \times 10^6 M_\odot$ (see Table 1). Despite using more dust than is allowed, Model 1 provides insufficient emission at $\lambda < 2 \text{ mm}$.

Because Model 1 violates the dust abundance limit, we try fitting the DL07 model to the same data, but now limiting $U_{\text{min}} \geq 0.4$. The resulting Model 2 has a total dust mass that does not exceed the upper limit in Table 1, but the quality of the fit to the SED is somewhat worse than for Model 1, with an even larger deficiency at $\lambda > 2 \text{ mm}$ (see Figure 2(b)).

5. SPINNING DUST

We can add a spinning dust component to raise the emission in the 20–60 GHz range. The spinning dust emission in the diffuse ISM of the Galaxy peaks near 30 GHz. What is expected for spinning dust in the SMC?

The anomalous microwave emission in the Galaxy is thought to be dominated by spinning dust, with the emission coming primarily from the smallest PAHs in the size distribution, as these are the only ones that spin as fast as $\sim 30 \text{ GHz}$ in the diffuse ISM (CNM, WNM, or diffuse WIM). The small-size end of the size distribution is thought to be determined by the size below which nanoparticles (molecules) would be destroyed by the interstellar $h\nu < 13.6 \text{ eV}$ UV background, $\sim 25 \text{ C atoms}$ (Allamandola et al. 1989; Gahathakura & Draine 1989). The threshold for grain survival is relatively insensitive to modest variations in the UV spectrum and intensity, hence we expect the lower size cutoff in the SMC to be similar to that in the Galaxy. The $5–18 \mu\text{m}$ spectrum of PAH emission from the SMC (Sandstrom et al. 2010) is broadly similar to that in normal star-forming galaxies in the SINGS sample (Smith et al. 2007), aside from an overall weakening due to lower PAH abundance, but the band ratios suggest a shift to smaller sizes (Sandstrom et al. 2012).

Thus, we expect the spinning dust emission from the SMC to be similar to that in the Galaxy, with the strength scaled down in proportion to the inferred PAH abundance. A slight shift to higher frequencies seems possible.

Draine & Lazarian (1998a, 1998b) argued that the anomalous microwave emission in the Galaxy, with an observed emissivity per H nucleon $[j_{\text{rot}}(30 \text{GHz})/n_{\text{H}}]_{\text{MW}} \approx 1 \times 10^{-17} \text{ Jy sr}^{-1} \text{ cm}^2 \text{ Hz}^{-1}$, is primarily rotational emission from the PAH population. The PAH abundance is measured by $q_{\text{PAH}}$, the fraction of the total dust mass contributed by PAHs with $<10^3$ C atoms. Dust in the solar neighborhood is thought to have $q_{\text{PAH}} \approx 4.6\%$. Li & Draine (2002) found that $q_{\text{PAH}}$ in the SMC was spatially variable and, on average, much lower than in the Milky Way. Sandstrom et al. (2010) confirmed this, finding a mean $\langle q_{\text{PAH}} \rangle \approx 0.6\%$. We expect the dust/gas ratio in the SMC to be lower by about a factor $\sim Z_{\text{SMC}}/Z_\odot \approx 0.25$. Therefore, the PAH abundance per H is down by about a factor $\sim (0.6/4.6) \times 0.25 = 0.033$. Thus, we estimate the spinning dust...
emission in the SMC to be

\[
\left[ \frac{j_{v}^{(sd)}(30 \text{GHz})}{n_{H}} \right]_{\text{SMC}} \approx 0.033 \times 1 \times 10^{-17} \text{ Jy sr}^{-1} \text{ cm}^{2} \text{ H}^{-1} \\
\approx 3.3 \times 10^{-19} \text{ Jy sr}^{-1} \text{ cm}^{2} \text{ H}^{-1}
\]

\[
\Delta F_{v}^{(sd)}(30 \text{GHz}) \approx \left[ \frac{j_{v}^{(sd)}(30 \text{GHz})}{n_{H}} \right]_{\text{SMC}} \times \frac{M_{H}}{m_{H}} D^{-2} \approx 5 \text{ Jy}.
\]

In Figure 2, we have added an emission component with a spectrum

\[
\Delta F_{v}^{(sd)} = \Delta F_{v}^{(sd)}(v_{0}) \left( \frac{v}{v_{0}} \right)^{2} \exp[1 - (v/v_{0})^{2}]
\]

representative of what is expected for spinning dust. The SMC SED suggests that the spinning dust peak may be near ~40 GHz. If we set \( v_{0} = 40 \text{ GHz} \) and \( \Delta F_{v}^{(sd)}(40 \text{GHz}) = 5 \text{ Jy} \)—consistent with the estimate in Equation (8)—the 20–50 GHz observations are accounted for, as seen in Figure 2.

While spinning dust appears able to account for the observed 20–50 GHz emission, the emission between 50 and 300 GHz remains much stronger than expected. Bot et al. (2010) suggest that the 50–300 GHz excess could also be due to spinning dust emission. However, theoretical models of rotational emission from small grains (Draine & Lazarian 1998b; Ali-Haïmoud et al. 2009; Hoang et al. 2010, 2011; Silsbee et al. 2011) predict little rotational emission above ~100 GHz unless high densities and warm gas temperatures are present in the emitting regions. For example, Draine & Lazarian (1998b, see Figure 13) calculated the spinning dust emission from a model photodissociation region (PDR) with \( n_{H} = 10^{5} \text{ cm}^{-3} \), \( T = 300 \text{ K} \), illuminated by a radiation field \( U \approx 3000 \). The PDR was assumed to have abundances of small grains relative to big grains reduced by a factor of five relative to diffuse clouds in the solar neighborhood, approximating the observed reduction in \( \phi_{\text{PAH}} \) in the SMC. Viewed face-on, the total IR luminosity/area \( L_{\text{TR}}/A \approx 3.6 \times 10^{4} \text{ erg cm}^{-2} \text{ s}^{-1} \). The spinning dust emission for this model peaked near 110 GHz, with \( (vL_{v}^{(sd)})_{100 \text{GHz}} = 7.4 \times 10^{-7} \text{ erg cm}^{-2} \text{ s}^{-1} \). Thus, \( L_{\text{TR}}/(vL_{v}^{(sd)})_{100 \text{GHz}} \approx 1.5 \times 10^{7} \). At 100 GHz, the model in Figure 2(b) has a deficit \( \Delta F_{v} \approx 25 \text{ Jy} \), corresponding to \( (vL_{v}^{(sd)})_{100 \text{GHz}} = 4 \times 10^{-7} \text{ erg cm}^{-2} \text{ s}^{-1} \). To account for this would require PDRs with a luminosity \( L_{\text{IR}} = 4.5 \times 10^{10} \text{ L}_{\odot} \)—completely inconsistent with the observed \( L_{\text{IR}} = 1 \times 10^{5} \text{ L}_{\odot} \). We therefore conclude, in agreement with Planck Collaboration et al. (2011b), that spinning dust cannot account for the observed 50–200 GHz emission in the SMC. Here, we consider magnetic dust grains as an alternative.

6. SMC DUST MODELS INCLUDING MAGNETIC DUST

Because magnetic materials have enhanced absorption at microwave and submm frequencies, it is of interest to see whether the mm- and cm-excess seen in the SMC could be due in part to thermal emission from magnetic grain materials. In Figures 3 and 4, we model the observed emission from the SMC as the sum of three components: “normal” dust (the amorphous silicate, graphite, and PAH model of DL07), a population of magnetic grains, and spinning dust. In each case, the spinning dust contribution is assumed to peak at 40 GHz, with the peak magnetic grains reduced by a factor of five relative to diffuse clouds in the solar neighborhood, approximating the observed reduction in \( \phi_{\text{PAH}} \) in the SMC. Viewed face-on, the total IR luminosity/area \( L_{\text{TR}}/A \approx 3.6 \times 10^{4} \text{ erg cm}^{-2} \text{ s}^{-1} \). The spinning dust emission for this model peaked near 110 GHz, with \( (vL_{v}^{(sd)})_{100 \text{GHz}} = 7.4 \times 10^{-7} \text{ erg cm}^{-2} \text{ s}^{-1} \). Thus, \( L_{\text{TR}}/(vL_{v}^{(sd)})_{100 \text{GHz}} \approx 1.5 \times 10^{7} \). At 100 GHz, the model in Figure 2(b) has a deficit \( \Delta F_{v} \approx 25 \text{ Jy} \), corresponding to \( (vL_{v}^{(sd)})_{100 \text{GHz}} = 4 \times 10^{-7} \text{ erg cm}^{-2} \text{ s}^{-1} \). To account for this would require PDRs with a luminosity \( L_{\text{IR}} = 4.5 \times 10^{10} \text{ L}_{\odot} \)—completely inconsistent with the observed \( L_{\text{IR}} = 1 \times 10^{5} \text{ L}_{\odot} \). We therefore conclude, in agreement with Planck Collaboration et al. (2011b), that spinning dust cannot account for the observed 50–200 GHz emission in the SMC. Here, we consider magnetic dust grains as an alternative.

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Metallic iron nanoparticles are introduced in Figure 3. We consider Fe grain temperatures of 40 K (Figure 3(a)) and 20 K (Figure 3(b)). If the Fe nanoparticles are, for the most part, free-fliers heated by typical starlight, then \( T \approx 40 \text{ K} \) is expected (see Figure 4 of Draine & Hensley 2012). If, on the other hand, the Fe nanoparticles are inclusions in larger composite grains, then the \( T \approx 20 \text{ K} \) temperature is appropriate, consistent with the temperature of the “normal” dust. In each case, the Fe grain abundance is adjusted to reproduce most of the observed emission near 100 GHz, then a model using DL07 dust is used to provide the additional emission required to reproduce the observed SED at shorter wavelengths, and finally a spinning
dust component peaking at 40 GHz is added to bring the model into agreement with the 20–50 GHz observations.

We also consider nanoparticles of maghemite (Figure 4(a)) and magnetite (Figure 4(b)). For these, we assumed temperatures $T \approx 17$ K consistent with being inclusions within non-magnetic dust grains.

The model with maghemite (Figure 4(a)) has $M_{Fe} = 2.2 \times 10^5 M_{\odot}$ of Fe in maghemite (total maghemite mass $3.1 \times 10^5 M_{\odot}$) and the model with magnetite (Figure 4(b)) has $M_{Fe} = 2.2 \times 10^5 M_{\odot}$ of Fe in magnetite (total magnetite mass $3.0 \times 10^5 M_{\odot}$). The Fe mass, and total dust mass, does not violate the mass budget (see Table 1). We conclude that the observed mm-wave emission from the SMC can be accounted for by models with reasonable abundances of normal dust plus metallic Fe, maghemite, magnetite, or some combination of these three materials.

If the nanoparticles are present as inclusions in larger grains, then it is clear that the size distribution of the larger particles can be adjusted to be compatible with the observed wavelength-dependent extinction in the SMC. But is it possible for the bulk of the interstellar Fe to be in free-flying nanoparticles? We have calculated the extinction contribution in the optical and UV, assuming that 100% of the Fe is in particles of a single type, and using dielectric functions for Fe, Fe$_3$O$_4$, and $\gamma$-Fe$_2$O$_3$ from Draine & Hensley (2012). Figure 5 shows the calculated extinction per H, together with the observed extinction in the SMC Bar (Gordon et al. 2003). The observed extinction does not rule out the hypothesis that most of the Fe is in free-flying nanoparticles.

Nevertheless, we consider it most likely that the bulk of the magnetic nanoparticles would be present as inclusions in larger grains, since we know that most of the grain mass is in grains with radii $a \gtrsim 0.1 \mu m$.

7. DISCUSSION

7.1. Alternative Models

The far-infrared and submm opacity of interstellar grain materials remains poorly understood. The “conventional dust model” opacity used in Section 4 is based on the emission from dust in diffuse Galactic H I observed by FIRAS (Wright et al. 1991; Finkbeiner et al. 1999). Some authors have proposed that the opacity of amorphous dust grains may depend strongly on temperature, with hotter dust having smaller $\beta \equiv d \ln \kappa_\nu/d \ln \nu$ and larger opacities at $\lambda > 100 \mu m$ (Boudet et al. 2005; Meny et al. 2007; Paradis et al. 2011). However, laboratory studies (Boudet et al. 2005; Coupeaud et al. 2011) show little variation in opacity over the actual 10–30 K temperature range for the interstellar dust dominating the emission. It is not yet clear whether the “$T - \beta$ relation” seen in astronomical observations (Paradis et al. 2010) is real or is an artifact of the combined effects of measurement noise (Shetty et al. 2009a) and variations in dust temperature along the sightline (Shetty et al. 2009b).

Planck Collaboration et al. (2011b) fit the SMC SED by adjusting the parameters of the “two-level system” (TLS) model for temperature-dependent opacities, with the temperature fixed at $T = 18.9 K$. However, the best-fit TLS parameters appear to fall outside the range of what has been thus far seen in laboratory studies. Thus, these models, while reproducing the observed
photometry, may not correspond to the absorption properties of interstellar dust.

7.2. Solid-phase Iron in Low-metallicity Galaxies

At submm–mm frequencies, the SED of the SMC is significantly less steep than the SED of normal-metallicity spiral galaxies, including the Galaxy. If the enhanced emission of the SMC at mm-wavelengths is due to Fe or Fe oxide grains, then such grains must account for a larger fraction of the dust mass in the SMC than in normal-metallicity spirals: conditions in the SMC must be in some way more favorable for their production or survival than in normal star-forming galaxies.

Spitzer Space Telescope observations of globular clusters have detected excess infrared emission from the most luminous giant stars, indicative of dusty winds. In many cases, the IR spectrum of the infrared excess is dominated by a featureless continuum at $\lambda > 8 \mu m$. Globular clusters where such featureless spectra have been seen include 47 Tuc (McDonald et al. 2011a), NGC 362 (Boyer et al. 2009), and Omega Cen (McDonald et al. 2011b); these three clusters have metallicities [Fe/H] $\approx -0.7, -1.3, -1.5$, respectively (Harris 1996, 2010 edition). The featureless continuum has therefore instead been attributed to thermal emission from metallic Fe grains (McDonald et al. 2010, 2011a, 2011b). Thus, low-metallicity asymptotic giant branch stars provide a possible source for metallic iron or Fe oxide grains in low-metallicity galaxies such as the SMC.

The iron-rich ejecta of Type Ia supernovae constitute a second potential source of iron grains (Dwek 1998). However, to date there is no evidence of dust formation in SN Ia ejecta, despite sensitive searches toward the Tycho and Kepler supernova remnants (Gomez et al. 2012).

Type II supernovae are known to form dust in the ejecta in at least some cases (Sugerman et al. 2006; Matsuura et al. 2011), and it is conceivable that Fe-rich portions of the ejecta might condense metallic Fe or Fe oxides. Rho et al. (2008) made models to reproduce the 5–38 $\mu m$ spectra of the Cas A ejecta; their global model had 0.028 $M_\odot$ of dust, of which 37% was metallic Fe.

Baron et al. (1977) observed that lunar soil grains have an increase in the concentration of Fe near the surface, with some of the Fe in metallic form. These surface layers (“rims”) reflect exposure of the grains to cosmic rays and the solar wind. “Inclusion-rich rims” consist of an amorphous silica-rich matrix with abundant metallic Fe inclusions, typically <10 nm in diameter (Keller & McKay 1997). Inclusion-rich rims are compositionally distinct from the host grain, and are thought to have formed by deposition of atoms from vapors produced by nearby sputtering or impact events. In the laboratory, irradiation of olivine by 4 keV He ions is observed to lead to alteration of the surface layers, with formation of metallic Fe nanoparticles (Dukes et al. 1999; Carrez et al. 2002; Loeffler et al. 2009). Metallic Fe nanoparticles are found as inclusions in interplanetary dust particles known as GEMS (“Glasses with Embedded Metals and Sulfides”; Bradley 1994). Thus, it is reasonable to consider that some of the Fe in interstellar grains may be in metallic Fe inclusions.

Fe-rich grain material is injected into the ISM from stellar sources; as seen above, this may include metallic Fe. Additional conversion of gas-phase Fe to solids must take place in the ISM to account for observed low gas-phase abundance of Fe, particularly in view of the likely importance of grain destruction by sputtering in supernova blastwaves (Draine & Salpeter 1979a; Jones et al. 1994; Draine 2009): it has been estimated that “stardust” (material condensed in stellar outflows) accounts for only a small fraction—perhaps 10%—of the interstellar grain mass in the Galaxy (Draine 1990, 2009), and this is likely the case for all galaxies where a substantial fraction of the refractory elements (Mg, Si, Fe) is in grains. In such galaxies, including the SMC, the bulk of the grain material must have undergone conversion from gas to solid in the ISM. The character of the interstellar dust will therefore be largely determined by interstellar processing.

Sputtering by energetic H and He can alter the composition of interstellar dust. Sputtering yields have been discussed by a number of authors (e.g., Draine & Salpeter 1979b; Tielens et al. 1994). For a composite material, sputtering yields for H and He will be larger for the lighter elements in the target, and sputtering will therefore leave the surface layers enriched in heavy elements (such as Fe). The grain material that survives sputtering will therefore become Fe-rich, perhaps even metallic Fe. Studies of elemental depletions in the solar neighborhood indeed suggest that Fe is concentrated in grain cores (Fitzpatrick & Spitzer 1997; Jenkins 2009). Based on the observed depletion pattern toward Sk 155 in the SMC, Wity et al. (2001) suggested that much of the interstellar Fe in the SMC (at least on the sightline to Sk 155) is in the form of metallic Fe or Fe oxides.

Rates for grain growth by accretion are proportional to the metallicity, while rates for grain destruction by H and He sputtering are not. The balance between grain growth and destruction, and the composition of the extant material, will therefore depend on the metallicity of the ISM. This may account for the apparent difference in grain composition between normal-metallicity spirals (like the Milky Way) and low-metallicity dwarf galaxies such as the SMC.

7.3. High-frequency Magnetism and the Gilbert Equation

The models presented here use absorption cross sections $C_{abs}(\omega)$ for magnetic grains calculated following Draine & Hensley (2012), who used the Gilbert equation (Gilbert 2004) to model the frequency-dependent magnetic response of Fe, maghemite, and magnetite. The Gilbert equation uses an adjustable dimensionless parameter $\alpha_G$ to characterize the dissipation. We have adopted $\alpha_G \approx 0.2$ for the purposes of discussion, but the existing experimental literature employs a range of values of $\alpha_G$. If $\alpha_G$ were to be smaller than 0.2, then the opacity at 100 GHz would be reduced, and the mass of Fe required to reproduce the observed emission of the SMC would correspondingly increase. If $\alpha_G \lesssim 0.05$, then using magnetic grain models to explain the $\sim 3$ mm emission would be ruled out by abundance constraints.

7.4. Polarization

Based on starlight polarization studies, the magnetic field in the SMC appears to lie primarily in the plane of the sky, with substantial large-scale coherence (Mao et al. 2008, 2012). While our understanding of the physics of grain alignment remains incomplete, dust grains in the SMC are expected to be partially aligned with long axes tending to be perpendicular to the local
magnetic field $B_0$. Electric-dipole emission, which dominates for $\lambda \lesssim 500 \mu m$, will be polarized with $E_\nu \perp B_0$.

As seen above, magnetic dipole emission from magnetic nanoparticles may become important for $\lambda \gtrsim 1$ mm. The polarization of the magnetic dipole emission has been discussed by Draine & Hensley (2012). If the magnetic nanoparticles are free-fliers, and are aligned by a Davis–Greenstein-like mechanism, then the magnetic dipole emission will be polarized in the same sense as the FIR emission, but the fractional polarization may be even larger than that of the FIR emission (see Figure 9 of Draine & Hensley (2012)). Alternatively, if the magnetic nanoparticles are present as randomly oriented inclusions within larger aligned grains, the magnetic dipole emission will be polarized with $E_\nu \parallel B_0$. As a result, the fractional polarization may decrease by a factor $\sim 2$ as the frequency decreases from 200 GHz to $\sim 40$ GHz, and for magnetite, maghemite, or Fe spheroids, the net polarization undergoes a reversal (i.e., changes from $E_\nu \perp B_0$ to $E_\nu \parallel B_0$) near $\sim 15$ GHz (see Figure 10 of Draine & Hensley 2012).

Planck will measure the polarization at 30, 44, 70, 143, 217, and 353 GHz. Unfortunately, there are two additional factors that will complicate interpretation of the dependence of polarization fraction on frequency:

1. Emission from spinning dust becomes increasingly important with decreasing frequency, peaking near $\sim 40$ GHz. If this emission component is minimally polarized, as predicted (Lazarian & Draine 2000), it will cause the fractional polarization to decrease with decreasing frequency in the 60–100 GHz region.

2. There may be more than one grain type contributing to the “normal” electric dipole” emission at long wavelengths, as in the mixtures of silicate and carbonaceous grains considered by Draine & Fraisse (2009). In this case, even the “normal” electric dipole emission alone may have the fractional polarization depending significantly on frequency. In the models of Draine & Fraisse (2009), the fractional polarization is predicted to increase with decreasing frequency.

Actual reversal of the polarization below $\sim 15$ GHz would be an unambiguous indication of magnetic dipole emission from magnetic inclusions, but this may be overwhelmed by the increasing importance of synchrotron emission (polarized with $E_\nu \perp B_0$) as the frequency falls below 10 GHz.

8. SUMMARY

The principal conclusions of this paper are as follows:

1. We show (see Figures 3 and 4) that the SED of the SMC can be approximately reproduced by a mixture of “normal” dust (illuminated by a plausible range of radiation intensities) plus emission from a population of small ($a \lesssim 0.01 \mu m$) magnetic nanoparticles. We consider three magnetic materials: metallic Fe, magnetite Fe$_3$O$_4$, and maghemite $\gamma$-Fe$_2$O$_3$. It appears that any of these three materials, or a combination of them, can provide enough emission at $\lambda > 1$ mm so that a combination of “normal dust,” spinning dust, and magnetic dust can account for the observed SED of the SMC.

2. If conditions in the SMC are conducive to a large fraction of the interstellar Fe being in magnetic nanoparticles, other low-metallicity galaxies may also have mm-wave emission dominated by magnetic dipole emission.

3. While it seems natural for the magnetic nanoparticles to be inclusions in larger grains, the observed extinction does not rule out the possibility that the magnetic nanoparticles might be independent free-fliers.

4. If the magnetic nanoparticles are present as randomly oriented inclusions in larger silicate grains, then the polarization is expected to fall as the frequency decreases below $\sim 200$ GHz. It may be possible to test this prediction with measurements by Planck of the polarized emission from the SMC.

5. Our models are based on high-frequency magnetic properties as estimated by Draine & Hensley (2012) using the Gilbert equation. Laboratory studies of the high-frequency ($\nu \gtrsim 100$ GHz) magnetic properties of metallic Fe and Fe oxides are needed to improve our understanding of magnetism at high frequencies.

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