On the magnetic fields of Be/X-ray pulsars in the Small Magellanic Cloud

N.R. Ikhsanov$^{1,2,3}$ and S. Mereghetti$^4$

$^1$ Pulkovo Observatory, Pulkovskoe shosse 65-1, St. Petersburg, 196140, Russia
$^2$ Special Astrophysical Observatory BAS, Nizhnii Arkhyz, 369167 Russia
$^3$ Saint-Petersburg State University, St. Petersburg, 198504 Russia
$^4$ INAF, IASF-Milano, via E.Bassini 15, Milano I-20133, Italy

Accepted: 2015 September 9; Received: 2015 July 8; Published: MNRAS 454, 3760-3765 (2015)

ABSTRACT

We explore the possibility of explaining the properties of the Be/X-ray pulsars observed in the Small Magellanic Cloud (SMC) within the magnetic levitation accretion scenario. This implies that their X-ray emission is powered by a wind-fed accretion on to a neutron star (NS) which captures matter from a magnetized stellar wind. The NS in this case is accreting matter from a non-Keplerian magnetically levitating disc which is surrounding its magnetosphere. This allows us to explain the observed periods of the pulsars in terms of spin equilibrium without the need of invoking dipole magnetic fields outside the usual range $\sim 10^{11} - 10^{13}$ G inferred from cyclotron features of Galactic high-mass X-ray binaries. We find that the equilibrium period of a NS, under certain conditions, depends strongly on the magnetization of the stellar wind of its massive companion and, correspondingly, on the magnetic field of the massive companion itself. This may help to explain why similar NSs in binaries with similar properties rotate with different periods yielding a large scatter of periods of the accretion-powered pulsar observed in SMC and our galaxy.

Key words: accretion, accretion discs – pulsars: general – stars: winds, outflows – X-rays: binaries.

1 INTRODUCTION

The Small Magellanic Cloud (SMC) contains a large number of accreting pulsars in high mass X-ray binaries (HMXBs). These sources, being at a well known, virtually uniform distance and with small interstellar absorption, constitute an ideal sample for population studies of neutron star (NS) binaries (Haberl & Pietsch 2004; Shytkovskiy & Gilfanov 2005; Laycock et al. 2010).

Klus et al. (2014) have recently reported parameters of 42 Be/X-ray binaries in the SMC observed with the Rossi X-ray Timing Explorer (RXTE) satellite over a time span of 14 yr. These systems, most of which are transients, contain pulsars in which the X-ray emission is powered by wind-fed accretion on to a magnetized NS. The average spin periods of these pulsars are in the range $P_s \sim 2.37 - 1323$ s and change at an average rate $|\dot{P}| \sim (0.02 - 620) \times 10^{-2}$ s yr$^{-1}$. Their orbital periods range from about 4 to 500 d.

Klus et al. (2014) estimated the magnetic fields of these NSs considering the situation in which they accrete matter from a Keplerian disc and rotate close to their equilibrium spin period. In this case, the estimated fields of the majority of the stars (including all those with $P_s > 100$ s) turn out to be over the quantum critical value $B_{cr} = m_e^2 c^3 / e \hbar \approx 4.4 \times 10^{13}$ G. Here $m_e$ and $e$ are the mass and electric charge of an electron, $c$ is the speed of light and $\hbar$ is the reduced Planck constant. Alternatively, if these NSs are not close to spin equilibrium, their inferred magnetic fields are smaller than $\sim 10^{10}$ G. Such results are rather unexpected since the majority of NSs in our Galaxy, including accretion-powered pulsars in HMXBs in which the magnetic field is measured from the cyclotron resonance scattered features, have magnetic fields between $10^{11}$ and $10^{13}$ G (see, e.g., Revnivtsev & Mereghetti 2015). An attempt to invoke currently used quasi-spherical accretion scenarios did not help much to improve the situation either, leading to estimated magnetic fields in excess of $10^{13}$ G.

It is not unusual that the magnetic fields evaluated from the spin parameters of NSs in Galactic HMXBs significantly exceed those measured through observations of their cyclotron resonance features. As recently indicated by Ikhsanov et al. (2014), this inconsistency may reflect an oversimplification of currently used wind-fed accretion scenarios, in which the magnetic field of the matter captured by the NS from its environment is neglected. The incorporation of the fossil magnetic field of the accreting matter into the model leads, under certain conditions, to a different accretion regime which is referred to as magnetic levitation accretion. In this scenario, which is briefly outlined in the next section, accretion occurs through a non-Keplerian magnetically levitating disc.

© 2015 The Authors

E-mail: n.ikhsanov@spbu.ru (NRI); sandro@iasf-milano.inaf.it (SM)
2 MAGNETIC LEVITATION ACCRETION

We consider an HMXB, with orbital period $P_{orb}$, composed of a magnetized NS rotating with spin period $P_s$ and a massive early-type star, which underfills its Roche lobe and loses matter through a stellar wind. The X-ray emission of the system is powered by wind-fed accretion on to the NS. This implies that the NS captures matter from the wind at a rate $\dot{M}_w = \pi r_r^2 P_0 v_0$, where $r_r = 2GM_*/v_r^2$ is the Bondi radius, $M_*$ is the NS mass, $v_0$ is its velocity in the frame of the wind, and $P_0 = \rho_0 r_r$ is the density of matter in the region of interaction. The captured matter moves towards the NS forming an accretion flow, which interacts with the stellar magnetic field and confines the magnetosphere within the radius $r_{mag}$, where the flow pressure is balanced by the pressure of the NS magnetic field. The accreting matter penetrates into the field at the magnetospheric boundary and, finally, falls on to the stellar surface at the magnetic pole regions by moving along the magnetic field lines.

The analysis of this accretion scenario reported by Ikhsanov & Finger (2012) indicates that the structure of the accretion flow, as well as the appearance of the accretion-powered source, strongly depend on the physical conditions of the matter captured at the Bondi radius, which, in general, possess some angular momentum and magnetic field. Under these conditions, the structure of the accretion flow beyond the magnetosphere can be treated in the following basic approximations: (i) a spherically symmetrical or quasi-spherical flow, (ii) a Keplerian disc, and (iii) an ML-disc. A key parameter which allows us to determine which of these situations applies is the relative velocity of the NS with respect to surrounding matter, $v_{rel}$.

The spherically symmetrical accretion occurs if the gas surrounding the NS does not possess angular momentum and is non-magnetized. The captured matter in this case moves towards the NS in the radial direction with the free-fall velocity, $v_{ff}(r) = (2GM_*/r)^{1/2}$ in a spherically symmetrical fashion. Its density scales with the radius as $\rho(r) = 9\rho_0/4\pi r^2 v_{ff}$ and the ram pressure is

$$P_{ram}(r) = \rho(r)v_{ff}^2(r) \propto r^{-5/2}. \quad (1)$$

The minimum distance to which the spherical flow can approach a NS with dipole magnetic moment $\mu$ is $r \gg r_h$ (Arons & Lea 1976; Elsner & Lamb 1977), where

$$r_h = \left( \frac{\mu^2}{9\pi(2GM_*)} \right)^{2/7} \quad (2)$$

is the Alfven radius which is defined by equating the ram pressure of the free-falling gas, with the magnetic pressure due to dipole magnetic field of the NS, $P_{mag} = \mu^2/(2\pi r^6) \propto r^{-6}$.

The structure of a non-magnetized accretion flow deviates from spherically symmetrical if the captured matter possesses angular momentum. The process of mass accretion in this case is accompanied by the accretion of angular momentum, which in a binary system with the orbital angular velocity $\Omega_{orb} = 2\pi/P_{orb}$ occurs at the rate $J = \xi \Omega_{orb} r_h^2 \dot{M}_w$ (Illarionov & Sunyaev 1975). Here $\xi$ is the parameter accounting for dissipation of angular momentum due to density and velocity gradients in the accreting non-magnetized gas (see e.g. Ruffert 1999, and references therein). The angular velocity of matter in this so called quasi-spherical accretion flow scales with the radius as

$$\Omega(r) = \xi \Omega_{orb} \left( \frac{r}{r_h} \right)^2, \quad (3)$$

and the azimuthal component of the dynamical pressure of the flow,

$$E_\phi(r) = \rho_0 \xi^2 \Omega_{orb}^2 \frac{r_h^4}{G M_\text{NS}} \frac{r}{r_h}^{7/2} \propto r^{-7/2}, \quad (4)$$

increases more rapidly than the ram pressure. The accretion proceeds in a quasi-spherical fashion up to the circularization radius

$$r_{circ} = \frac{\xi^2 \Omega_{orb}^2 r_h^4}{G M_\text{NS}}, \quad (5)$$

at which condition $E_\phi(r) = E_{crit}(r)$ is satisfied. The angular velocity of the accreting matter, $\Omega(r)$, at this radius reaches the Keplerian angular velocity, $\Omega_k = (r/2GM_*)^{1/2}$, and the accretion flow switches into a Keplerian accretion disc (Pringle & Rees 1972; Shakura & Sunyaev 1973).

The accretion picture may differ from that presented above if the matter captured by the NS at the Bondi radius is magnetized. As long as the Alfvén velocity, $v_A(r) = B(r)/[\mu_0 \sigma_\text{mag}(r)]^{1/2}$, in the accreting matter is smaller than the free-fall velocity, the magnetic field of the accreting gas, $B$, does not influence significantly the flow structure. Therefore, the captured matter initially follows ballistic trajectories forming a quasi-spherical accretion flow in which the angular momentum and magnetic flux are almost conserved. However, the magnetic pressure in the free-falling gas increases rapidly,

$$E_{mag}(r) = \frac{B^2(r)}{8\pi} \propto r^{-4}, \quad (6)$$

and reaches the ram pressure at the Shvartsman radius (Shvartsman 1971)

$$R_{sh} = \beta_0 r_h^{2/3} \left( \frac{c_{sh}}{v_{rel}} \right)^{4/3}, \quad (7)$$

which is defined by equating the magnetic to ram pressure. Here $\beta_0 = \rho_0 r_h = \mu_0 \sigma_\text{mag} r_h/B_0^2$ is the ratio of thermal to magnetic pressure in the captured matter at the Bondi radius, $c_{sh} = c_A(e_{sh})$ is the sound speed and $B_0 = B(r_{sh})$ is the magnetic field in the accreting matter. The flow at this radius is converted into a non-Keplerian ML-disc in which the accreting matter is confined by its own magnetic field (for discussion see Bisnovatyi-Kogan & Ruzmaikin 1976; Igumenshchev, Narayan, & Abramowicz 2003). The accretion inside the ML-disc proceeds on the time-scale of the magnetic flux dissipation and, in the general case, can be treated in a diffusion approximation. The value of the effective diffusion coefficient strongly depends on the configuration of the magnetic field in the disc and its stability. It ranges from the Bohm diffusion coefficient, if the magnetic field annihilation in the disc is governed by dissipative instabilities and magnetic reconnections, up to much larger values if the field configuration is interchange unstable (for discussion see Igumenshchev 2009; Tchekhovskoy, Narayan and McKinney 2011; Dexter et al. 2014, and references therein).

Thus, a quasi-spherical accretion on to a NS in a wind-fed HMXB occurs if the Alfvén radius is larger than both the circularization and the Shvartsman radii. The angular momentum and magnetic field of the accreting material in this case are too small to
significantly influence the flow structure before the ballistic trajectories of the accreting matter are truncated by the magnetic field of the NS. Solving the inequality $r_c > \max [r_{\text{acc}}, R_{\text{sh}}]$ for $v_{\text{rel}}$ one finds

$$v_{\text{rel}} \geq \begin{cases} v_{\text{ac}}, & \text{for } R_{\text{sh}} < r_c, \\ v_{\max}, & \text{for } R_{\text{sh}} > r_c, \end{cases}$$

(8)

where (Ikhsanov 2007)

$$v_{\text{ac}} \simeq 160 \text{ km s}^{-1} \frac{15^{1/4} \tau_{0.2}^{1/14} M_{11/28}}{P_{351}^{11/14}} \left( \frac{r_{30}}{10 \text{ km s}^{-1}} \right)^{2/5}$$

(9)

and (Ikhsanov & Beskrovnaya 2012; Ikhsanov & Finger 2012)

$$v_{\max} \simeq 460 \text{ km s}^{-1} \times \frac{P_{30}^{1/5}}{P_{535}^{6/35}} m^{12/35} \left( \frac{\xi_{c}^{2}}{10 \text{ km s}^{-1}} \right)^{2/5}.$$  

(10)

Here $\mu_{0} = \mu / (10^{30} \text{ G cm}^{-3})$ is the dipole magnetic moment of a NS with surface magnetic field $B_{\text{s}}$ and radius $R_{\text{sh}}$, $m = M_{\text{BH}}/1.4 M_{\odot}$, $\beta_{35} = \beta/10^{3}$, $P_{30} = P_{\text{orb}}/50 \text{ d}$, and the parameter $\xi_{c} = \xi/0.2$ is normalized according to Ruffert (1999). The radius of the magnetosphere, within this scenario, is comparable or slightly exceeds the Alfve\"{n}n radius (Arons & Lea 1976; Elsner & Lamb 1977), and accretion beyond the magnetospheric boundary proceeds in the form of a free-falling gas or a hot turbulent spherical envelope (Lamb et al. 1977; Ikhsanov 2001, 2003).

A Keplerian accretion disc in a wind-fed HMXB can form if the circularization radius exceeds both the Alfve\"{n}n and Shvartsman, radii. Solving inequality $r_{\text{acc}} > \max [r_{c}, R_{\text{sh}}]$ for $v_{\text{rel}}$ one finds

$$v_{\text{rel}} \leq \begin{cases} v_{\text{ac}}, & \text{for } R_{\text{sh}} < r_{c}, \\ v_{\max}, & \text{for } R_{\text{sh}} > r_{c}, \end{cases}$$

(11)

where (Ikhsanov, Kim & Beskrovnaya 2015)

$$v_{\text{ac}} \simeq 80 \text{ km s}^{-1} \frac{12^{1/7} P_{20}^{1/7}}{P_{535}^{6/35}} m^{1/14} \left( \frac{\xi}{10 \text{ km s}^{-1}} \right)^{-2/7}.$$  

(12)

Finally, a non-Keplerian ML-disc can form in a wind-fed HMXB if the Shvartsman radius is larger than both, the Alfve\"{n}n and circularization radii. Solving inequality $R_{\text{sh}} > \max [r_{c}, r_{\text{acc}}]$ for $v_{\text{rel}}$ yields

$$v_{\text{ac}} < v_{\text{rel}} < v_{\max}.$$  

(13)

The inequality $v_{\text{ac}} < v_{\max}$ is satisfied if $\beta_{0} < \beta_{\text{max}}$, where

$$\beta_{\text{max}} \simeq 164 \frac{c_{\sigma}^{5/4}}{P_{20}^{1/4} P_{535}^{3/10}} m^{1/14} \left( \frac{\xi_{c}^{2}}{10 \text{ km s}^{-1}} \right)^{2}.$$  

(14)

This indicates that the magnetic levitation accretion scenario occurs if the fossil magnetic field in the matter captured by the NS is $B_{l}(\xi_{c}) > B_{\text{max}}$, where

$$B_{\text{max}} \simeq \left( \frac{2 \mu_{0} v_{\sigma}^{2} c_{\sigma}^{2}}{(GM_{\odot})^{2} \beta_{\text{max}}} \right)^{1/2} \simeq 6 \times 10^{-4} \text{ G} \times$$

(15)

\begin{eqnarray*}
\times \frac{\xi_{c}^{2/7} P_{30}^{1/4} m^{1/14} P_{535}^{3/10}}{P_{30}^{1/4} P_{535}^{3/10}} \left( \frac{\nu_{\text{rel}}}{100 \text{ km s}^{-1}} \right)^{3/2},
\end{eqnarray*}

The matter in an ML-disc approaches the NS until the radius

$$r_{\text{max}} = \left( \frac{c_{\sigma}^{2}}{16 \sqrt{2} \epsilon_{K}} \right)^{2/13} \frac{a_{\sigma}^{13}}{r_{30}^{2/13} \eta_{13}^{11/13}} \left( \frac{G M_{\odot}^{1/3}}{r_{30}^{1/3} \epsilon_{K}^{1/13}} \right)^{1/13},$$

(16)

where the pressure exerted by the disc on to the stellar magnetosphere is equal to the magnetic pressure due to the NS dipole field and the rate of diffusion of the accreting matter into the stellar field is equal to the mass capture rate by the star from its environment (for discussion see Ikhsanov 2012; Ikhsanov et al. 2014). Here $m_{p}$ is the proton mass, $k_{B}$ is the Boltzmann constant and $T_{0}$ is the temperature of the matter at the inner radius of the disc. The parameter $\alpha_{e} = D_{\text{eff}}/D_{q}$ is the ratio of the effective coefficient of diffusion of the accreting matter into the stellar field at the magnetospheric boundary, $D_{\text{eff}}$, to the Bohm diffusion coefficient, which in the considered case can be expressed as $D_{q} = c_{\sigma}^{2} r_{\text{max}} / (32 \mu)$. Numerical simulations of the diffusion process and measurements of the rate at which the solar wind penetrates into the magnetosphere of the Earth suggest that $\alpha_{e} \sim 0.01$–1 (Gosling et al. 1991). The matter being diffused into the stellar field flows along the magnetospheric field lines and reaches the NS surface at the magnetic pole regions.

The possibility of explaining the parameters of the SMC Be/X-ray pulsars within the quasi-spherical and the Keplerian disc accretion scenarios has been already discussed by Khus et al. (2014). Here we explore the possibility that these pulsars accrete matter from an ML-disc. In the next section we evaluate the equilibrium period of an NS in this scenario and present the expected Corbet ($P_{s}$ versus $P_{\text{orb}}$) diagram in Section 4.

### 3 EQUILIBRIUM PERIOD

The equation governing the spin evolution of an NS accreting matter from an ML-disc reads

$$2\pi \nu = K_{s} + K_{t} + K_{s},$$

(17)

where $I$ is the moment of inertia and $\nu = 1/P_{s} = \omega_{s}/2\pi$ is the spin frequency of the NS. The first term in the right-hand side of this equation,

$$K_{s} = \Re \ell(\nu_{\text{max}}) \Re \omega_{s} r_{\text{max}}^{2},$$

(18)

is the rate at which angular momentum is transferred to the NS by the matter flowing inside the magnetosphere. Here $\ell(\nu_{\text{max}}) \equiv r_{\text{max}} \times (\nu_{\text{max}} \omega_{s})$ is the specific angular momentum of matter in the magnetopause at the rotational equator. This matter, which penetrates into the stellar field at the magnetospheric boundary, correlates with the NS and flows towards its surface along the field lines. $K_{s}$ has a positive sign and represents the minimum possible spin-up torque exerted on to a star which is surrounded by a magnetosphere of radius $r_{\text{max}}$ and accretes matter onto its surface at a rate $\Re \ell$.

The second term (Ikhsanov 2012; Ikhsanov et al. 2014),

$$K_{t} = \left( \frac{\xi_{c}}{r_{\text{max}} c_{\sigma}} \right)^{1/2} \left( \frac{\Omega(\nu_{\text{max}})}{\omega_{s}} - 1 \right),$$

(19)

accounts for the angular momentum exchanged between the star and the disc at the magnetospheric boundary (here $k_{t}$ is a dimensionless parameter of order unity). The sign of this term depends on the ratio between the angular velocity of matter at the inner radius of the disc, $\Omega(\nu_{\text{max}})$, and the angular velocity of the NS. The last term, $K_{s}$, accounts for the angular momentum exchanged between the NS and the disc at radius $r > r_{\text{max}}$. Under the conditions of interest ($d\Omega/d\nu \equiv 0$), this term is smaller than $K_{s}$ at least by a factor $r_{\text{max}}^{1/2}$. Therefore, its contribution is relatively small and we neglect it in the following.

The equilibrium period, $P_{\text{eq}}$, is defined by equating the total torque exerted on the NS (right-hand side of equation 17) to zero, which, using equations (18) and (19), yields

$$P_{\text{eq}} \simeq P_{s}(\nu_{\text{max}}) \left[ 1 - \frac{1}{2k_{t}^{2}} \left( \frac{\nu_{\text{max}}}{\nu_{s}} \right)^{2} \right],$$

(20)

where $P_{s}(\nu_{\text{max}}) = 2\pi/\Omega(\nu_{\text{max}})$.
This equation suggests that the angular velocity of the NS in spin equilibrium exceeds the angular velocity of the matter at the inner radius of the disc by a factor of \(1 - (1/\sqrt{2} k_t) (r_{ma} / r_K)^{7/2}\). The torque \(K_t\) in this case has a negative sign and tends to spin-down the star. It, however, is compensated by the spin-up torque \(K_a\) and thus, the total torque exerted on the NS is zero.

Evaluating the ratio

\[
\left(\frac{r_{ma}}{r_K}\right)^{7/2} \sim 10^{-3} \alpha_B^{7/13} \mu_{10}^{5/13} m^{10/13} \gamma_{15}^{-1/13} \gamma_{6}^{-7/13},
\]

(21)

one finds that the expression in the brackets in the conditions of interest (\(10^{-3} \ll k_t \ll 1\)) is close to unity (here \(T_{sh} = 0.6^6 K\) is normalized to the temperature of optically thick gas irradiated by the pulsar emission, see, e.g. Hickox, Narayan and Kallman 2004). This indicates that the angular velocity of the NS in spin equilibrium is close to the angular velocity of the matter at the inner radius of the disc. This allows us for simplicity to approximate the equilibrium period of the NS by \(P(t_{ma})\).

The analysis of the transport of angular momentum across the ML-disc is rather complicated and beyond the scope of this paper. The angular momentum extracted from the NS can be stored in the disc (Sunyaev & Shakura 1977; D’Angelo & Spruit 2012) or transferred out from the disc by Alfvén waves. Here we simply assume that the angular velocity of the matter in the disc scales with the radius as \(\Omega_K (r) \propto (R_K / r)^{\gamma}\), where \(\gamma\) is a free parameter, which in the general case is limited to \(1 \leq \gamma \leq 2\). The angular velocity of matter at the inner radius of the disc can be expressed as

\[
\Omega_K (r_{ma}) = \Omega_K (R_K) \left(\frac{R_K}{r_{ma}}\right)^{\gamma},
\]

(22)

where

\[
\Omega_K (R_K) \approx \xi \Omega_{orb} \left(\frac{r_K}{R_K}\right)^2
\]

(23)

is the angular velocity of matter at the Shvartsman radius. This is derived by taking into account that the magnetic field of the accreting matter does not significantly influence the flow structure beyond the Shvartsman radius and the matter in the region \(R_K < r < r_K\) moves towards the NS quasi-spherically.

Putting equations (7), (16) and (23) into equation (22) and taking into account that the relative velocity in the considered case is \(\nu_{rel} = \xi \nu_{ma}\), with \(\xi < 1\), one finds

\[
P(t_{ma}) = 0.5 \frac{1.3^{10/13}}{2^\gamma} A_m P_{orb},
\]

(24)

where

\[
A_m = \xi^{-1} p_0^{4/5} c_{10}^{8/5} \mu_{10}^{1/5} \gamma_{15}^{-4/5} (GM_{_NS})^{1/5} \left(\frac{c m_2}{\sqrt{2} \alpha_{\gamma} k_{\gamma}}\right)^{2/13}
\]

(25)

\[a_1 = (208 - 50 \gamma)/455,\]

\[a_2 = (10 \gamma + 104)/455,\]

\[a_3 = (10 \gamma - 8)/3,\]

(26)

The value \(\gamma=2\) corresponds to conservation of angular momentum, \(\gamma=1.5\) to Keplerian rotation, \(\gamma=1\) to rotation with constant linear velocity, and \(\gamma=0\) to solid body rotation.

Finally, the value of the dimensionless parameter \(\xi\) in the general case lies in the interval \(\xi_{min} < \xi < 1\), where

\[
\xi_{min} = \begin{cases} \nu_{ma}/\nu_{ca}, & \nu_{ma} > \nu_{ca}, \\ \nu_{ca}/\nu_{ma}, & \nu_{ma} < \nu_{ca}, \end{cases}
\]

(26)

and \(\nu_{ca}\) is the orbital velocity of the NS.

4 APPLICATION TO THE SMC PULSARS

In this section we explore the possibility of explaining the spin properties of the SMC Be/X-ray pulsars in terms of the magnetic levitation accretion scenario described above. We assume that the NSs in these systems rotate close to the equilibrium period \(P_{eq} \approx P(t_{ma})\) given by equation (24) and accrete matter from an ML-disc. This implies that the relative velocity of the NSs in the frame of stellar wind of their companions meets the condition \(\nu_{ma} < \nu_{ca} \approx \nu_{ma}\) and \(\beta_0 < \beta_{max}\) expressed by equation (14). Since the accretion process in an ML-disc is fully controlled by the magnetic field of the accreting matter itself, we consider the case of rigid rotation of the disc by setting \(\gamma = 0\).

The minimum possible value of the equilibrium period, \(P_{min}\), which an NS can acquire within the magnetic levitation accretion scenario can be derived from equation (24), by setting \(\beta_0 = \beta_{max}\) and, correspondingly, \(\xi = 1\). This yields

\[
P_{min}^6 = 14 s \times \mu_{30}^{6/7} \gamma_{15}^{-3/7} m^{-3/7},
\]

(27)

where \(\gamma_{15}\) is the average mass accretion rate normalized to \(10^{15}\) g s\(^{-1}\).

In Fig. 1 the values of \(P_{min}^6\) are compared to the observed values of \(P\), and \(P_{obs}\) for representative values of \(\mu \sim (10^{30})\) G cm\(^3\) solid lines; \(10^{39}\) G cm\(^3\) dashed lines and \(\gamma_{15} \sim (10^{14} 10^{15})\) g s\(^{-1}\). The corresponding lines indicate the minimum possible equilibrium period of an NS which captures matter from a relatively slow, moderately magnetized stellar wind in the magnetic levitation accretion scenario.

The maximum possible equilibrium period, \(P_{max}\), can be evaluated from equation (24) by setting \(\nu_{ca} = 1\) and \(\nu_{ma} < \nu_{ca}\), which for the case \(\nu_{ma} < \nu_{ca}\) (see equation 26):

\[
P_{max}^6 \sim 20 s \times \mu_{30}^{15/7} \gamma_{15}^{15/7} \beta_{0}^{-6/7} \gamma_{24}^{24/7} m^{-8/7},
\]

(28)

Putting this value into equation (24) one finds

\[
P_{max}^6 \sim 20 s \times \mu_{30}^{15/7} \gamma_{15}^{15/7} \beta_{0}^{-6/7} \gamma_{24}^{24/7} m^{-8/7},
\]

(29)

The function \(P_{max}^6 = P_{max}^6(P_{obs})\) is shown by the dot-dashed line in Fig. 1. The maximum equilibrium period of an NS which accretes from a magnetized slow wind does not depend on the magnetic field of the NS itself and on the X-ray luminosity of the pulsar. However, it is a strong function of the sound speed in the surrounding matter and, therefore, it can exceed the value given by equation (29) if the temperature of the stellar wind exceeds \(10^7\) K.

Fig. 1 shows that practically all the pulsars reported by Klus et al. (2014) have spin-period values smaller than \(P_{max} = P_{max}(P_{obs})\) and lying above the lines of \(P_{min}\) corresponding to \(\mu \sim 10^{29-30}\) G cm\(^3\) and accretion rates consistent with the long-term average luminosities of these sources. This suggests that the observed spin periods can be explained within the magnetic levitation accretion scenario with surface magnetic fields of the NSs in the canonical interval \(B_{ms} \sim 10^{11-10^{13}}\) G.
5 DISCUSSION

We find that the observed spin periods of the SMC Be/X-ray pulsars are in a range consistent with the values expected for the equilibrium periods of NSs with magnetic fields of $B \sim 10^{11-13}$ G and accreting from an ML-disk. The assumption that the NSs in these systems are spinning close to an equilibrium value is supported by the fact that they show alternate episodes of spin-up and spin-down, which do not change $P_s$ significantly on the long term. We believe that the equilibrium period is set by the average accretion rate experienced by these NS during the long time intervals of quiescence (or low X-ray luminosity) between their bright outbursts. In fact these sources spend most of the time in such low-$\dot{M}$ conditions, resulting in X-ray luminosities well below the RXTE sensitivity limit of $\sim 10^{36}$ erg s$^{-1}$. For this reason we have adopted in Fig. 1 values of $\dot{M}$ corresponding to luminosities of $\sim 10^{34-35}$ erg s$^{-1}$.

The equilibrium period of an NS which accretes from a ML-disc tends to increase with the orbital period of a binary system (see equation 24). This, in particular, can be a reason for a lack of pulsars in the lower-right part of the Corbet plot. On the other hand, $P_{eq}$ also depends on several other parameters, such as the magnetic field and relative velocity of an NS, the mass accretion rate, and physical conditions in the stellar wind with which the NS interacts. The great diversity of possible combinations of these parameters is responsible for the large scatter of the observed spin periods in the Corbet plot. In this accretion regime, the magnetic field of the massive star plays an important role, with stronger fields leading to longer equilibrium periods of the pulsar.

Spectropolarimetric observations of O/B-type stars give evidence for a relatively strong magnetization of these objects (see, e.g. Walder, Folini & Meynet 2012, and references therein). The strength of the large-scale field at the surface of several of these objects has been measured in the range $\sim 500 - 5000$ G, and in some cases beyond 10 kG (Hubrig et al. 2006; Martins et al. 2010; Oksala et al. 2010). Some of the early type stars are surrounded by X-ray coronae which indicate the magnetic activity of these objects (Schulz et al. 2003). As most of these stars rotate relatively fast (see e.g. Rosen, Krumholz & Ramirez-Ruiz 2012, and references therein), the magnetic field in the wind is dominated by the toroidal component which scales with the radius $\propto r^{-1}$.

A similar situation is realized in the solar wind in which the magnetic field at a distance of 1 au is $B_{sun} \sim 10^{-5}$ G and the parameter $\beta$ is close to the equipartition value, $\beta \sim 1$ (Mullan & Smith 2006). Following this similarity one can suggest that the surface large-scale magnetic field of massive stars in the considered systems is a factor of $B_{sun}/B_{eq} \sim 50$ larger than the surface large-scale magnetic field of the Sun and can be as large as a few hundred Gauss. A smaller magnetization of these stars cannot be also excluded if the dynamo action applies in their outflowing discs. The fact that periods of the considered pulsars are much shorter than the maximum possible period predicted by our model may indicate that the average value of $\beta_0$ exceeds unity and hence, the stellar wind of early spectral type stars is less magnetized than the solar wind. The observed range of periods of the pulsars ($\sim 1 - 1000$ s) in this case can be explained in terms of variation of $\beta_0$ parameter from system to system within an order of magnitude.

Our study confirms the conclusion of Klus et al. (2014) that all of the considered pulsars are situated in a relatively slow wind. This
is consistent with current views on the mass outflow process of Be stars, in which the stellar wind at the equatorial plane is dominated by a dense outflowing disc. The radial velocity of matter in the disc is comparable or even smaller than the orbital velocity of the NS (Okazaki & Negueruela 2001).

We finally note that our results apply also to the Be/X-ray pulsars in our Galaxy, which show a distribution in the $P_{\text{orb}} - P_{\text{s}}$ similar to that of the SMC sources. This supports the view that the properties and evolution of HMXBs in the SMC and in our Galaxy share a common nature and are governed by similar physical processes.

ACKNOWLEDGEMENTS

We would like to thank anonymous referee for very useful and stimulating comments. NRI thanks INAF at Milano for kind hospitality and acknowledges support of the Russian Scientific Foundation under the grant no. 14-50-00043. This work has been partially supported through financial contribution from the agreement ASI/INAF I/037/12/0 and from PRIN INAF 2014.

REFERENCES

Arons, J., Lea, S.M. 1976, ApJ, 207, 914
Bisnovatyi-Kogan, G.S., Ruzmaikin, A.A., 1976, ApSS, 42, 401
Elsner, R.F., Lamb, F.K. 1977, ApJ, 215, 897
D’Angelo, C.R., Spruit, H.C. 2012, MNRAS, 420, 416
Dexter, J., McKinney, J.C., Markoff, S., Tchekhovskoy, A. 2014, MNRAS, 440, 2185
Gosling, J.T., Thomsen, M.F., Bame, S.J., Elphic, R.C., Russell, C.T. 1991, J. Geophys. Res. 96, 14097
Haberl, F., Pietsch, W. 2004, A&A, 414, 667
Hickox, R.C., Narayan, R., Kallman, T.R. 2004, ApJ, 614, 881
Hubrig, S., Yudin, R.V., Schöller, M., Pogodin, M.A. 2006, A&A, 446, 1089
Igumenshchev, I.V. 2009, ApJ, 702, L72
Igumenshchev, I.V., Narayan, R., Abramowicz, M.A. 2003, ApJ, 592, 1042
Ikhsanov, N.R. 2001, A&A, 375, 944
Ikhsanov, N.R. 2003, A&A, 399, 1147
Ikhsanov, N.R. 2007, MNRAS, 375, 698
Ikhsanov, N.R. 2012, MNRAS, 424, L39
Ikhsanov, N.R., Beskrovnaya, N.G. 2012, Astron. Rep., 56, 589
Ikhsanov, N.R., Finger, M.H. 2012, ApJ, 753, 1
Ikhsanov, N.R., Likh, Yu.S., Beskrovnaya, N.G. 2014, Astron. Rep., 58, 376
Ikhsanov, N.R., Kim, V.Yo., Beskrovnaya, N.G. 2015, Astron. Rep., 59, 25
Illarionov, A.F., Sunyaev, R.A. 1975, A&A, 39, 185
Klus, H., Ho, W.C.G., Coe, M.J., Corbet, R.H.D., Townsend, I.J. 2014, MNRAS, 437, 3863
Lamb, F.K., Fabian, A.C., Pringle, J.E., Lamb, D.Q. 1977, ApJ, 217, 197
Lacycoy, S., Zezas, A., Hong, J., Drake, J.J., Antoniou, V. 2010, ApJ, 716, 1217
Martins, F., Donati, J.-F., Marcolino, W.L.F., Bouret, J.-C., Wade, G.A., Escolano, C., Howarth, I.D. 2010, MNRAS, 407, 1423
Mullan, D.J., Smith, C.W. 2006, Sol. Phys., 234, 325
Okazaki, A.T., Negueruela, I. 2001, A&A, 377, 161
Oksala, M.E., Wade, G.A., Marcolino, W.L.F., Grunhut, J., Bohleuder, D., Manset, N., Townsend, R.H.D. 2010, MNRAS, 405, 51
Pringle, J.E., Rees, M.J. 1972, A&A, 21, 1
Revnivtsev, M., Mereghetti, S. 2015, Space Sci. Rev., preprint arXiv:1411.5843
Rosen, A.L., Krzeminski, M.R., Ramirez-Ruiz, E. 2012, ApJ, 748, 97
Ruffert, M. 1999, A&A, 346, 861
Schulz, N.S., Canizares, C., Hueneremoeder, D., Tibbets, T. 2003, ApJ, 595, 365
Shakura, N.I., Sunyaev, R.A. 1973, A&A, 24, 337
Sunyaev, R.A., Shakura, N.I. 1977, Sov. Astron. Lett., 3, 138
Shytovskiy, P., Gilfanov, M. 2005, MNRAS, 362, 879
Shvartsman, V.F. 1971, SvA, 15, 377
Tchekhovskoy, A., Narayan, R., McKinney, J. 2011, MNRAS, 418, L79
Walder, R., Polini, D., Meynet, G. 2012, Space Sci. Rev., 166, 145

This paper has been typeset from a TeX/LaTeX file prepared by the author.