Constructive and Destructive Interference of Kerker-type Scattering in an Ultra-thin Silicon Huygens Metasurface

Xia Zhang, Jing Li, John F. Donegan, and A. Louise Bradley
School of Physics, CRANN and Amber, Trinity College Dublin, Ireland
(Dated: January 12, 2021)

High refractive index dielectric nanoparticles have provided a new platform for exotic light manipulation through the interference of multipole modes. The Kerker effect is one example of a Huygens source design. Rather than exploiting interference between the electric dipole and magnetic dipole, as in many conventional Huygens source designs, we explore Kerker-type suppressed backward scattering mediated by the dominant electric dipole, toroidal dipole and magnetic quadrupole. These modes are provided by a designed and fabricated CMOS compatible ultra-thin Silicon nanodisk metasurface with a suppressed magnetic dipole contribution, and verified through multipole decomposition. The non-trivial substrate effect is considered using a semi-analytical transfer matrix model. The model successfully predicts the observed reflection dip. By applying a general criterion for constructive and destructive interference, it is shown that while constructive interference occurs between the electric and toroidal dipole contributions, the experimentally observed suppressed backward Kerker-type scattering arises from the destructive interference between backward scattered contributions due to the total electric dipole and the magnetic quadrupole. Our study paves the way towards new types of Huygens sources or metasurface design, such as for peculiar transverse Kerker scattering.

I. INTRODUCTION AND MOTIVATION

Huygens’ Principle states that all points of a wave front of light can be regarded as a new source of secondary waves that expand in every direction. Metasurfaces encompass an array of elements, each of which behaves as secondary sources, providing a platform for control of the radiation [1–4]. The light transmitted, reflected or refracted through a metasurface can be manipulated to obtain a desired direction, wavefront, phase and polarization. This control is realized by designing the nanoresonator shape, size, material, as well as their geometrical arrangement in one unit cell and period [5, 6]. A dielectric metasurface can have much higher efficiency compared with a plasmonic counterpart, which suffer from ohmic losses. Additionally, a dielectric metasurface, or an array of dielectric nanoresonators, sustains overlapping resonant multipolar resonances [7–9]. The interplay of multipolar resonances in a metasurface or a single nanoresonator provides another degree of freedom for light tailoring, such as the Kerker effect, the anti-Kerker effect [10–12], and transverse Kerker scattering [13–15]. Kerker-type scattering, or highly suppressed backward scattering, attracts much interest as it enables a non-radiative when dipole [12] is denoted as TED. The TED can be invisable or non-radiative when p = −ikT, referred to as an “anapole mode” [25–27]. A recent review on the TD and how it can be used for exotic light manipulation can be found in reference [28]. An ideal non-radiating anapole mode arises from the complete destructive interference of the radiation from the ED and the TD [29–31]. There have been many experimental reports of anapole modes identified through their near-field distribution of opposite closed loop circulating current densities [32]. In the broader context, it is defined as low-radiation or suppressed scattering [33] arising from partial destructive interference. However, it is also found, by tuning the geometrical factors in high refractive index cylindrical nanostructures, that constructive interference between the scattering contributions from the ED and TD can be achieved, termed the super-dipole state [12]. It is worth noting that an ED can also manifest as a dip in far-field...
scattering profile of a single nanodisk [34] or a single nanowire [35]. Additionally, under most circumstances where the ED moment and TD moment do not generate scatter fields of comparable amplitude, it is difficult to conclude from the far-field radiation pattern how the scattered contributions interfere with each other. This is the same principle as the visibility of interference, where a clear visible bright and dark pattern, or ideal unity visibility, requires that the interfering waves share the same amplitude and simultaneously meet the phase relationship. If a disparity of amplitude exists between the interfering two waves, the interference is more difficult to discern. Therefore, the experimentally observed near-field scattering pattern with a circulating electric field profile and/or a suppressed far-field scattering is insufficient to conclude on the existence of super-dipole or anapole modes. Multipole decomposition is thus pivotal to understanding the mechanisms that produce the far-field scattered power.

The amplitude and phase of the electromagnetic radiation generated by each of the multipole contributions determines the observed far-field scattered power. Once the modes can be identified, the question arises as to whether the scattered radiation contributions interfere constructively or destructively. One method that is used is to compare the amplitude of the ED/TD and TED contributions [18, 25]. This can clearly demonstrate the destructive interference mechanisms but is insufficient to conclude constructive interference. If the amplitude of the coherent sum of the ED and TD amplitudes, TED, is smaller than ED or TD, it can be concluded that destructive interference exists. However, constructive interference cannot be concluded from an increase of the TED amplitude compared to ED or TD amplitudes. Here we present an approach to identify constructive and destructive interference through analysis of the scattered power of the multipole modes. Additionally, in contrast to the most studies of interference arising due to the ED and MD, we performed our study on a specifically designed ultra-thin Si metasurface with suppressed MD contribution but ED, TD and magnetic quadruple (MQ) mode so that we can explore the interference between their scattered contributions. We also include the effects of the substrate on the measured optical properties of the metasurface.

II. EXPERIMENT, SIMULATION AND MODEL

Silicon (Si) nanodisk metasurfaces are fabricated on a Si-on-insulator (SOI) wafers (45 nm top Si thickness, 150 nm buried oxide thickness, Soitec). Electron-beam lithography is performed on spin-coated PMMA 950 layer (A3, 3000 rpm) by Electron beam (Elionix ELS 7700), followed by the development in MIBK:IPA 1:3. A 20 nm thickness of chromium (Cr) layer was deposited by e-beam evaporator (Temescal). After lift-off process in hot Remover 1165, a Cr layer was used as a hardmask, the pattern was transferred to the SOI substrate by Inductively Coupled Plasma Etching (ICP) through the top Si layer with an over-etched thickness of (10±3) nm BOX layer, verified by Ellipsometry. The thickness of SiO2 is 140 nm. The Cr mask was finally removed using a commercial Cr etchant from Sigma.

In order to achieve a metasurface with a suppressed MD and dominant TED and MQ contributions, arrays of ultra-thin Si nanodisks with a height of 45 nm and radii varying between 120 nm to 170 nm are fabricated. The thickness of SiO2 is 140 nm. The period in the x and y directions is 500 nm. A scanning electron microscopy image of one metasurface is shown in the inset, with a scale bar corresponding to 500 nm. A normally incident plane wave propagating in the z direction and polarized along the x-axis, \( E_{\text{inc}} = E_0 \text{e}^{i(kz-\omega t)} \mathbf{x} \), interacts with the metasurface. (b) Electric field map within one period for a nanodisk with \( r = 170 \, \text{nm} \) at a wavelength of 686 nm corresponding to the reflection dip wavelength 686 nm. The field map has an anapole-like pattern. (c) The measured and (d) numerically simulated reflection coefficient of the Si nanodisk metasurfaces with nanodisk radii of 120 nm to 170 nm.

FIG. 1. (a) Schematic of the periodic Si nanodisk metasurface. The thickness of SiO2 is 140 nm. The scanning electron microscopy image of one metasurface is shown in the inset, with a scale bar corresponding to 500 nm. A normally incident plane wave propagating in the z direction and polarized along the x-axis, \( E_{\text{inc}} = E_0 \text{e}^{i(kz-\omega t)} \mathbf{x} \), interacts with the metasurface. (b) Electric field map within one period for a nanodisk with \( r = 170 \, \text{nm} \) at a wavelength of 686 nm corresponding to the reflection dip wavelength 686 nm. The field map has an anapole-like pattern. (c) The measured and (d) numerically simulated reflection coefficient of the Si nanodisk metasurfaces with nanodisk radii of 120 nm to 170 nm.
linearly polarized along the $x$ axis and the wavevector $k$ is along the $z$ axis. The wavelength-dependent real and imaginary parts of refractive index and permittivity is obtained from fitting the experimental data in reference [36]. The simulation area is $500 \times 500 \times 6000$ nm$^3$ and the mesh size is 2.5 nm. The simulation is performed with periodic boundary conditions in the $x$ and $y$ directions and the perfectly matched layers in the $z$ direction.

As seen in Fig. 1(c) there is a clear dip in the experimentally observed reflection spectra, that shifts to higher wavelengths with increasing nanodisk radius. The reflection dip indicates the suppressed backward scattering or Kerker-type scattering. Fig. 1(d) shows excellent agreement of the numerically simulated spectra with the experimental data. Slight broadening of the measured spectra is observed due to inhomogeneously broadening from fabrication imperfection and non-perfect normal incidence in the measurement. As the disk radius is varied from 120 nm to 170 nm, the aspect ratio, defined as the ratio of height to diameter, is changed between 0.13 to 0.18. In contrast to most work on manipulating interferences between the ED and MD, these ultra-thin metasurfaces are the key to obtaining a suppressed MD and dominant ED, TD and MQ modes. The electric field distribution shown in Fig. 1(b) for a metasurface with a nanodisk of radius 170 nm indicates interference arising from the ED and TD mode contributions [34, 37, 38]. As stated earlier, excitation of the ED-alone can also manifest a dip in scattered radiation profile [34]. In order to explore the presence of super-dipole or anapole modes and to gain further insight into the nature of the interfering modes, multipole decomposition is performed.

According to the standard expansion method, we consider the decomposition of the multipolar modes up to quadrupole modes by integrating over the nanodisk volume [12].

$$p = \int \epsilon_0(\epsilon_{Sl} - 1)E(r)dr$$

$$T = -\frac{i\omega}{10k} \int \epsilon_0(\epsilon_{Sl} - 1) |(r \cdot E(r))r - 2r^2E(r)|dr$$

$$m = -\frac{i\omega}{2} \int \epsilon_0(\epsilon_{Sl} - 1) |r \times E(r)|dr$$

$$Q = 3 \int \epsilon_0(\epsilon_{Sl} - 1) |rE(r) + E(r)r - \frac{2}{3}(r \cdot E(r))\hat{U}|dr$$

$$M = \frac{\omega}{3i} \int \epsilon_0(\epsilon_{Sl} - 1) |(r \times E(r))r + r(r \times E(r))|dr$$

(1)

where $r$ is the coordinate vector with its origin placed at the center of nanodisk. $E(r)$ is the total electric field inside the nanoparticle at different position. $\epsilon_0$ is the vacuum permittivity; $\epsilon_{Sl}$ is the relative dielectric permittivity of the Si particle. $c$ is the light speed in vacuum; $\hat{U}$ is the $3 \times 3$ unity tensor; $p$, $T$, $m$, $Q$ and $M$ are the moments of ED, TD, MD, electric quadrupole (EQ) and MQ respectively.

Under linearly polarized, normally incident light, $E_{inc} = E_0 e^{i(kz - \omega t)} \hat{x}$, the effective contributing multipole moments to the far-field scattering are $p_x$, $T_x$, $m_y$, $Q_{xz}$ and $M_{yz}$ respectively [25]. $E_0$ is the amplitude of incident electric field, $k_0 = \frac{\omega}{c}$ is the wavevector in the incident medium, in this case air, and $\omega$ is the frequency of the optical field. The total scattered power includes the forward and backward scattering while the reflection spectra represent backward scattering only. The reflection coefficient is defined as $R = |r|^2$. In the case where only the Si nanodisks embedded in air is considered, the total contribution of the multipole moments to the re-
reflection coefficient, \( r_{MP} \), is expressed as

\[
r_{MP} = \frac{-ik_0}{2E_0A_0}(px + ik_0Tx - \frac{my}{c} + \frac{ik_0}{6}Q_{zz} - \frac{ik_0}{2c}M_{yy})
\]

where \( A \) is the area of one metasurface unit cell [25]. The contributions from multipole moments to the reflection coefficient \( r_{MP} = r_p + r_T + r_m + r_Q + r_M \), can be expressed as

\[
r_p = i k_0 p_x/(2E_0A_0),
\]

\[
r_T = -k_0^2 T_x/(2E_0A_0),
\]

\[
r_m = -k_0^2 m_y/(2E_0A_0),
\]

\[
r_Q = -k_0^2 Q_{zz}/(12E_0A_0) \quad \text{and}
\]

\[
r_M = \frac{k_0^2 M_{yy}}{(4cE_0A_0)}
\]

The amplitude and phase of each multipole mode determines how they interfere with each other and contribute to the far-field scattering. However, the practical metasurface studied here is on a SiO2/Si substrate, the substrate alters the induced electric field distribution within the nanodisk. Therefore, the reflection transmission coefficient of nanodisk is determined by the integration of the internal electric field within in the particle sitting on the substrate [39, 40]. Additionally, since the studied geometry is a stratified layer, including metasurface/air gap/SiO2 buffer layer/Si layers, we followed the transfer matrix calculations proposed in Ref. [6, 41] to probe the physics behind the reflection dip, which takes into account Fabry-Perot type multiple reflections within each layer. In the transfer matrix formalism, each layer is considered as a decoupled in-line optical element, where the light interaction is specified by its reflection coefficient \( r \) and transmission coefficient, \( t \). The reflection coefficient of overall structure is determined as

\[
R = \frac{|r_{MP}(e^{i\varphi_1} + r_{11}r_{22}e^{i\varphi_2}) + (t_{MP}^2 - r_{MP}^2)(r_{11}e^{-i\varphi_2} + r_{22}e^{-i\varphi_1})|^2}{e^{i\varphi_1} + r_{11}r_{22}e^{i\varphi_2} - r_{MP}(r_{11}e^{-i\varphi_2} + r_{22}e^{-i\varphi_1})}
\]

where \( \varphi_1 = -(k_0d_0 + k_0s) \) and \( \varphi_2 = -(k_0d_0 - k_0s) \) respectively.

The reflection signal is a superposition of several contributing EM waves, including the effective EM multipolar scattered wave generated by nanodisk and also light reflected from the SiO2/Si substrate. The light reflected from SiO2/Si substrate includes the contributions from the incident EM wave directly reflected from the SiO2 and Si substrates, together with Fabry-Perot type multiple reflections due the interfaces within the structure of both the incident and scattered light [6]. A schematic can be seen in Fig. 2 (a), where the reflection coefficient is calculated by the total transfer matrix, which takes into account the multiple reflections as well as the multipolar contribution determined by the induced internal electric field distribution of the nanodisk sitting on the substrate.

The results for the numerical simulation and semi-analytical calculation of the reflection coefficient, \( r \), are shown in Fig. 2 (b). The semi-analytical reflection coefficient, \( R \), is shown for two cases; i) the internal electric field distribution in the nanodisk for the multipole analysis, and subsequent determination of \( r_{MP} \) and \( t_{MP} \), has been calculated for the nanodisks embedded in air and ii) the electric field distribution is computed for the nanodisks sitting on the SiO2/Si substrate. The semi-analytical model for case (ii) and the numerically calculated reflection spectrum are in excellent agreement with each other and the experimentally measured reflection spectrum, which is also shown in Fig. 2 (b).

The spectral broadening of experimental measurement results from imperfect fabrication and non-perfect normal incidence in the measurement. A further comparison of the numerical simulations and semi-analytical calculations is presented in Figs. 2 (e) and (f). The semi-analytical reflection spectra show the same trend and features as the full numerical calculations over a wide range of disk radii from 100 nm to 240 nm. The amplitude and phase of all multipole contributions to the electric field reflection coefficient are shown in Fig. 2 (c) and (d), respectively. The dominant contributing multipole modes are the ED, TD and MQ. The contributions from the MD and EQ modes are significantly smaller. The
interference minimum at 686 nm is indicated by the grey dash lines in (b)(c) and (d) for more detailed inspection. It is worth noting that the minimum in reflection in Fig. 2 (b) is blue shifted with respect to the minimum in the amplitude of the reflection coefficient contribution from multipole modes, \( r_{MP} \), seen in Fig. 2 (c). This indicates the importance of the role played by the substrate.

The back-scattered power associated with each multipole moment can be expressed as \( |A|^2 \), where \( A \) is \( r_p \), \( r_T \), \( r_m \), \( r_Q \), or \( r_M \). However, as mentioned earlier the total reflected power depends on the interference of each component of the field, taking account of the amplitude and relative phase of the scattered fields. If we consider two contributions, \( A \) and \( B \), then the sum of their powers yields \( I_0 \) while taking account of the coherent superposition yields \( I_{int} \).

\[
I_0 = I_A + I_B = |A|^2 + |B|^2 \\
I_{int} = |A + B|^2 = |A|^2 + |B|^2 + 2|A||B|\cos(\varphi_A - \varphi_B)
\]

(4)

Under the circumstance that \( I_{int} > I_0 \), constructive interference is occurring between the two contributions while destructive interference exists when \( I_{int} < I_0 \). This is a general criterion to determine constructive or destructive interference and can be applied to any two multipole modes including even higher order modes.

As mentioned earlier, the contributions from the ED and TD can form a single contribution called the total electric dipole moment [12], or TED = \( r_p + r_T \). In order to explore how the ED and TD scattered fields interfere with each other, \( I_{int}^{TED} \) and \( I_0^{TED} \) are calculated using Eq.4 and are presented in Fig. 3 (a). It is clear that at the reflection minimum at 686 nm \( I_{int}^{TED} > I_0^{TED} \). This demonstrates that there is constructive interference between ED and TD contributions and the reflection dip does not result from an anapole-like mode generated by the ED and TD but rather the TED behaves as a superdipole at this wavelength and TED results in a increase of the far-field backward scattering. Additionally, it can be seen that there is a wide wavelength range over which there is constructive interference between the ED and TD contribution to the back-scattered radiation. This range is represented by the shaded area in Fig. 3 (a).

As seen in Fig. 2(c), the dominant multipole modes in the studied metasurface are ED, TD and MQ. The multipole reflection coefficient \( r_{MP} \) can be approximated as \( r_{MP} \approx r_{TED} + r_{MQ} \). The scattering power due to the TED and MQ modes can be seen in Fig. 3 (b). It is seen that \( I_{int}^{TED-M} < I_0^{TED-M} \) at 686 nm and there is destructive interference between TED and MD contributions. The wavelengths at which destructive interference exists are presented as the shaded area. Additionally, \( I_{int}^{TED-M} \neq 0 \) indicates there is only partial destructive interference and the back-scattered field due to the MQ could not totally compensate for the contribution from the TED but results in a decrease of total backward scattering power. Asymmetric scattering manipulation due to the ED and MD interference has been studied for almost 40 years [10]. Due to the inherent phase symmetry properties of MD and MQ modes in the forward and backward directions, where the MD displays odd phase symmetry and the MQ displays an even phase symmetry [15][19], the realization of dominant TED and MQ interference in this Letter paves the way towards symmetric scattering manipulation by employing only TED and MQ, such as the unusual transverse scattering, which simultaneously displays zero forward and zero backward scattering for the nanoresonator embedded in an isotropic medium [14]. Additionally, our study clearly demonstrated that the substrate effect is nontrivial in reshaping the far-field radiation pattern and must be taken into account for scattering pattern manipulation.

III. CONCLUSION

To conclude, we designed and fabricated an ultrathin Si nanodisk metasurface on a CMOS-compatible semiconductor-on-insulator wafer. Kerker-type suppressed backward scattering is observed through a minimum in the reflection spectrum and is seen to gradually red-shift with increasing disk radius. There is excellent agreement between the numerical simulation and experimental spectra. To probe the mechanism producing the suppressed backward scattering, multipole decomposition is performed. A semi-analytical model of backward scattering or reflection coefficient, taking into account the substrate- reflection contribution as well as the multipolar modes’ back-scattering is used and found to correspond well with experimental reflection spectrum. Multipole decomposition shows that the dominant modes in the designed Si nanodisk metasurface are the ED, TD
and MQ with suppressed MD mode. This provided a platform to investigate the Kerker-type scattering due to the ED, TD and MQ rather than conventional ED and MD interference. To address the fundamental issue of constructive or destructive interference of multipolar modes, a generalized criterion employing the amplitude, phase and power analysis is proposed. It is demonstrated that the observed suppressed back-scattering is mainly driven by the coherent interplay between the ED, TD and MQ contribution. The ED back-scattered radiation constructively interferes with that from the TD at the reflection minimum wavelength and the TED behaves as a super-dipole. The suppressed back scattered radiation is realized through destructive interference between the TED and MQ mode contributions. Due to distinct phase symmetry properties of MQ and MD in the forward and backward direction, our findings on TED-MQ interference will spur new Huygens source design or metasurface design for symmetric scattering tailoring, such as transverse scattering.

ACKNOWLEDGMENTS

We wish to acknowledge the support of Science Foundation Ireland (SFI) under Grant Numbers 16/IA/4550 and 17/NSFC/4918.

[1] C. L. Holloway, E. F. Kuester, J. A. Gordon, J. O’Hara, J. Booth, and D. R. Smith, An overview of the theory and applications of metasurfaces: The two-dimensional equivalents of metamaterials, IEEE Antennas Propag. Mag. 54, 10 (2012).
[2] C. Pfeiffer and A. Grbic, Metamaterial huygens’ surfaces: tailoring wave fronts with reflectionless sheets, Phys. Rev. Lett. 110, 197401 (2013).
[3] N. Yu and F. Capasso, Flat optics with designer metasurfaces, Nat. Mater. 13, 139 (2014).
[4] H.-T. Chen, A. J. Taylor, and N. Yu, A review of metasurfaces: physics and applications, Reports Prog. Phys. 79, 076401 (2016).
[5] F. Ding, A. Pors, and S. I. Bozhevolnyi, Gradient metasurfaces: a review of fundamentals and applications, Reports Prog. Phys. 81, 026401 (2017).
[6] V. E. Babicheva, M. I. Petrov, K. V. Baryshnikova, and P. A. Belov, Reflection compensation mediated by electric and magnetic resonances of all-dielectric metasurfaces, J. Opt. Soc. Am. B 34, D18 (2017).
[7] A. I. Kuznetsov, A. E. Miroshnichenko, M. L. Brongersma, Y. S. Kivshar, and B. Luk’yanchuk, Optically resonant dielectric nanostructures, Science 354 (2016).
[8] I. Staude and J. Schilling, Metamaterial-inspired silicon nanophotonics, Nat. Photonics 11, 274 (2017).
[9] V. E. Babicheva and A. B. Evlyukhin, Resonant lattice kerker effect in metasurfaces with electric and magnetic optical responses, Laser Photonics Rev. 11, 1700132 (2017).
[10] M. Kerker, D.-S. Wang, and C. Giles, Electromagnetic scattering by magnetic spheres, J. Opt. Soc. Am 73, 765 (1983).
[11] J.-M. Geffrin, B. García-Cámara, R. Gómez-Medina, P. Albella, L. Froué-Pérez, C. Eyraud, A. Litman, R. Vaillón, F. González, M. Nieto-Vesperinas, et al., Magnetic and electric coherence in forward-and-back scattered electromagnetic waves by a single dielectric subwavelength sphere, Nat. Commun. 3, 1 (2012).
[12] P. D. Terekhov, K. V. Baryshnikova, Y. A. Artemyev, A. Karabchevsky, A. S. Shalin, and A. B. Evlyukhin, Multipolar response of nonspherical silicon nanoparticles in the visible and near-infrared spectral ranges, Phys. Rev. B 96, 035443 (2017).
[13] A. Bag, M. Neugebauer, G. Woźniak Paweland Leuchs, and P. Banzer, Transverse kerker scattering for angstrom localization of nanoparticles, Phys. Rev. Lett. 121, 193902 (2018).
[14] H. K. Shamkhli, K. V. Baryshnikova, A. Sayansky, P. Kapitanova, P. D. Terekhov, P. Belov, A. Karabchevsky, A. B. Evlyukhin, Y. Kivshar, and A. S. Shalin, Transverse scattering and generalized kerker effects in all-dielectric mie- resonant metaoptics, Phys. Rev. Lett. 122, 193905 (2019).
[15] M. Liu and C. Zhao, Lattice invisibility effect based on transverse kerker scattering in 1d metalattices, J. Phys. D. Appl. Phys. 52, 495107 (2019).
[16] A. B. Evlyukhin, T. Fischer, C. Reinhardt, and B. N. Chichkov, Optical theorem and multipole scattering of light by arbitrarily shaped nanoparticles, Phys. Rev. B 94, 205434 (2016).
[17] I. Staude, A. E. Miroshnichenko, M. Decker, N. T. Fofang, S. Liu, E. Gonzales, J. Dominguez, T. S. Luk, D. N. Neshev, I. Brener, et al., Tailoring directional scattering through magnetic and electric resonances in subwavelength silicon nanodisks, ACS nano 7, 7824 (2013).
[18] P. D. Terekhov, K. V. Baryshnikova, A. S. Shalin, A. Karabchevsky, and A. B. Evlyukhin, Resonant forward scattering of light by high-refractive-index dielectric nanoparticles with toroidal dipole contribution, Opt. Lett. 42, 835 (2017).
[19] W. Liu and Y. S. Kivshar, Generalized kerker effects in nanophotonics and meta-optics, Opt. Express 26, 13085 (2018).
[20] A. Berkhout and A. F. Koenderink, A simple transfer-matrix model for metasurface multilayer systems, Nanophotonics 9, 3985 (2020).
[21] L. D. Kallepalli, D. Grojo, L. Charmasson, P. Delaporte, O. Utéza, A. Merlen, A. Sangar, and P. Torchio, Long range nanostructuring of silicon surfaces by photonic nanojets from microsphere langmuir films, J. Phys. D Appl. Phys. 46, 145102 (2013).
[22] V. Pacheco-Peña and M. Beruete, Photonic nanojets with mesoscale high-index dielectric particles, J. Appl. Phys. 125, 084104 (2019).
[23] M. Decker, I. Staude, M. Falkner, J. Dominguez, D. N. Neshev, I. Brener, T. Pertsch, and Y. S. Kivshar, High-efficiency dielectric huygens’ surfaces, Adv. Opt. Mater.
[24] R. Alaee, R. Filter, D. Lehr, F. Lederer, and C. Rockstuhl, A generalized kerker condition for highly directive nanoantennas, Opt. Lett. 40, 2645 (2015).
[25] P. D. Terekhov, V. E. Babicheva, K. V. Baryshnikova, A. S. Shalin, A. Karabchevsky, and A. B. Evlyukhin, Multipole analysis of dielectric metasurfaces composed of nonspherical nanoparticles and lattice invisibility effect, Phys. Rev. B 99, 045424 (2019).
[26] P. C. Wu, C. Y. Liao, V. Savinov, T. L. Chung, W. T. Chen, Y.-W. Huang, P. R. Wu, Y.-H. Chen, A.-Q. Liu, N. I. Zheludev, et al., Optical anapole metamaterial, ACS nano 12, 1920 (2018).
[27] A. E. Miroshnichenko, A. B. Evlyukhin, Y. F. Yu, R. M. Bakker, A. Chipouline, A. I. Kuznetsov, B. Luk’yanchuk, B. N. Chichkov, and Y. S. Kivshar, Nonradiating anapole modes in dielectric nanoparticles, Nat. Commun. 6, 1 (2015).
[28] M. Gupta and R. Singh, Toroidal metasurfaces in a 2d flatland, Rev. Phys. 5, 100040 (2020).
[29] L. Wei, Z. Xi, N. Bhattacharya, and H. P. Urbach, Excitation of the radiationless anapole mode, Optica 3, 799 (2016).
[30] E. Takou, A. C. Tasolamprou, O. Tsilipakos, and E. N. Economou, Dynamic anapole in metasurfaces made of sculptured cylinders, Phys. Rev. B 100, 1 (2019).
[31] J. A. Parker, H. Sugimoto, B. Coe, D. Eggena, M. Fujii, N. F. Scherer, S. K. Gray, and U. Manna, Excitation of nonradiating anapoles in dielectric nanospheres, Phys. Rev. Lett. 124, 097402 (2020).
[32] G. Grinblat, Y. Li, M. P. Nielsen, R. F. Oulton, and S. A. Maier, Enhanced third harmonic generation in single germanium nanodisks excited at the anapole mode, Nano Lett. 16, 4635 (2016).
[33] K. V. Baryshnikova, D. A. Smirnova, B. S. Luk’yanchuk, and Y. S. Kivshar, Optical anapoles: concepts and applications, Adv. Opt. Mater 7, 1 (2019).
[34] R. Wang and L. Dal Negro, Engineering non-radiative anapole modes for broadband absorption enhancement of light, Opt. Express 24, 19048 (2016).
[35] W. Liu, J. Zhang, B. Lei, H. Hu, and A. E. Miroshnichenko, Invisible nanowires with interfering electric and toroidal dipoles, Opt. Lett. 40, 2293 (2015).
[36] D. E. Aspnes and A. A. Studna, Dielectric functions and optical parameters of si, ge, gap, gaas, gasb, inp, inas, and insb from 1.5 to 6.0 ev, Phys. Rev. B 27, 985 (1983).
[37] Y. H. Fu, A. I. Kuznetsov, A. E. Miroshnichenko, Y. F. Yu, and B. Luk’yanchuk, Directional visible light scattering by silicon nanoparticles, Nat. Commun. 4, 1 (2013).
[38] S.-Q. Li and K. B. Crozier, Origin of the anapole condition as revealed by a simple expansion beyond the toroidal multipole, Phys. Rev. B 97, 245423 (2018).
[39] R. M. Bakker, D. Fermovakov, Y. F. Yu, D. Markovich, R. Paniagua-Domínguez, L. Gonzaga, A. Samusev, Y. Kivshar, B. Luk’yanchuk, and A. I. Kuznetsov, Magnetic and electric hotspots with silicon nanodimers, Nano Lett. 15, 2137 (2015).
[40] J. Tian, H. Luo, Y. Yang, Y. Ding, Y. Qu, D. Zhao, M. Qiu, and S. I. Bozhevolnyi, Active control of anapole states by structuring the phase-change alloy ge2sb2te5, Nat. Commun. 10, 1 (2019).
[41] H.-T. Chen, Interference theory of metamaterial perfect absorbers, Opt. Express 20, 7165 (2012).