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Spatial and Temporal Development of Incipient Dunes

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Abstract In zones of loose sand, wind-blown sand dunes emerge due to the linear instability of a flat sedimentary bed. This instability has been studied in experiments and numerical models but rarely in the field, due to the large time and length scales involved. We examine dune formation at the upwind margin of the White Sands Dune Field in New Mexico (USA), using 4 years of lidar topographic data to follow the spatial and temporal development of incipient dunes. Data quantify dune wavelength, growth rate, and propagation velocity and also the characteristic length scale associated with the growth process. We show that all these measurements are in quantitative agreement with predictions from linear stability analysis. This validation makes it possible to use the theory to reliably interpret dune-pattern characteristics and provide quantitative constraints on associated wind regimes and sediment properties, where direct local measurements are not available or feasible.

Plain Language Summary Dunes are the solar system’s ubiquitous landform, arising wherever wind blows over a loose sand bed. An aerodynamic theory for dune formation, which connects grain-scale movement to emergent dune pattern, has been developed for idealized scenarios. Yet this model has never been directly tested in nature, because of the complexities in observing dune formation at the initial stage. Here we report extensive topographic observations of the initiation, growth, and migration of real-world sand dunes. Moreover, we find a surprisingly precise agreement with the idealized aerodynamic theory. This robust confirmation of the theory for dune formation means that we may estimate wind conditions in remote places, including other planets, with confidence.

1. Introduction

The development of sand dunes, from incipient to mature bedforms, and their evolution, through interaction and coarsening processes, involve characteristic time and length scales that relate to elementary mechanisms of hydrodynamics and sediment transport (Courrech du Pont, 2015; Wiggs, 2013). Over loose granular beds, bedform emergence is driven by a hydrodynamic instability induced by the interaction between the sand bed, flow, and sediment transport (Charru et al., 2013). On the upstream side of a bump, erosion takes place as the flow accelerates. Reciprocally, the flow slows down on the downstream side where deposition occurs. However, the transition between erosion and deposition zones, associated with the location of the maximum of the sediment flux, does not necessarily take place at the crest of the bump. Spontaneous growth of such a bump—that is, instability—can therefore occur if its crest is located in the deposition zone (Kennedy, 1963). The streamwise offset between topography and sediment flux has two contributions (Andreotti et al., 2002; Claudin et al., 2013; Fournière et al., 2010; Kroy et al., 2002b). First, a hydrodynamic destabilization originates from the coupling between flow inertia and dissipation, which results in a maximum basal fluid shear stress located upstream of the crest (Hunt et al., 1988; Kroy et al., 2002a; Sykes, 1980). Second, the sand flux needs a characteristic length, called the saturation length, to adapt to a spatial change in shear stress (Andreotti et al., 2010; Durán et al., 2011; Pältz et al., 2013; Sauermann et al., 2001). This results in a stabilizing downstream lag of the maximum sand flux with respect to the maximum of the shear stress. These balancing processes give rise to the development and propagation of sand waves at a specific wavelength and propagation speed, associated with the most unstable mode of the pattern, with crests perpendicular to the dominant wind direction.
The early stage of growth and development of sedimentary ripples and dunes has been theoretically studied with linear stability analyses of coupled transport and hydrodynamic equations (Andreotti et al., 2002, 2012; Claudin & Andreotti, 2006; Colombini, 2004; Devauchelle et al., 2010; Durán Vinent et al., 2019; Fourrière et al., 2010; Gadal et al., 2019; Kennedy, 1963; Lagrée, 2003; Richards, 1980). These analyses predict the incipient pattern wavelength, propagation velocity, and growth rate as functions of model parameters, which encode the wind and grain characteristics. For the aeolian case in particular, the dune wavelength has been shown to be proportional to the saturation length. However, measuring the bed elevation together with sediment and fluid transport is difficult, thereby making the direct comparison between theory and field or experimental data rather challenging.

The aerodynamic and sediment transport responses have been investigated independently of each other, and separate measurements of the saturation length and the upwind shift of the shear stress have been carried out, in the field and in wind tunnel experiments (Andreotti et al., 2010; Claudin et al., 2013; Selmani et al., 2018). In contrast, few field studies addressing the early stage of aeolian dune growth are available in the literature (Baddock et al., 2018; Cooper, 1958; Elbelrhiti et al., 2005; Fryberger et al., 1979; Kocurek et al., 1992; Ping et al., 2014). First, in situ monitoring of the evolution of small amplitude bedforms is difficult due to the involved length and time scales (tens to hundreds of meters, days to months). Second, inherent wind variability—even in overall unidirectional dune fields—makes application of the theory challenging. Emergence of subaqueous sand ripples has also been experimentally investigated (Baas, 1999; Coleman & Melville, 1996; Fourrière et al., 2010; Langlois & Valance, 2007) and more generally the quantification of sedimentary bedforms in different environmental—including extraterrestrial—conditions in relation to hydrodynamics and sediment transport remains an active current subject of research (Durán Vinent et al., 2019; Gadal et al., 2019; Jia et al., 2017; Lapôtre et al., 2016, 2018).

In this paper, we study the upwind margin of the White Sands Dune Field, where the dune instability leads to spatially amplifying sand waves developing downstream (Ewing & Kocurek, 2010; Phillips et al., 2019). We follow the spatiotemporal evolution of incipient dunes and extract their wavelength and propagation velocity, as well as their temporal and spatial growth rates. We then show that these four quantities all quantitatively compare to the predictions of spatial linear stability analysis.

2. White Sands Dune Field

White Sands Dune Field is located in southern New Mexico, USA. The sand covers an area of about 400 km², resulting in the largest gypsum dune field on Earth. Dominant winds are mainly toward the northeast and shape the sedimentary bed into transverse and barchan dunes, progressively turning into parabolic dunes as the vegetation cover increases (Figures 1a and 1b) (Baitis et al., 2014; Jerolmack et al., 2012; McKee, 1966). Dunes emerge on the upwind margin (Figure 1c). There, the sediment is made of coarse, elongate, and angular grains (see Figure S2 in the supporting information), with a measured diameter \( D = 670 \pm 120 \mu m \) and a bulk density \( \rho_p = 2,300 \pm 100 \text{ kg m}^{-3} \). The saturation length, relevant in the process of dune emergence (see section 3), directly depends on these grain properties (Andreotti et al., 2010):

\[
L_{\text{sat}} = \frac{2.2 \rho_p}{\rho_l} d = 2.8 \pm 0.5 \text{ m},
\]

where \( \rho_l = 1.2 \text{ kg m}^{-3} \) is the air mass density in ambient conditions. As one moves further into the dune field, the grain diameter and angularity both decrease, due to abrasion and aeolian sorting (Jerolmack et al., 2011; Phillips et al., 2019). Because we restrict our analysis of the dune development to the first kilometer along the margin, the grain characteristics are assumed to be homogeneous. The grain roughness leads to a measured avalanche slope \( \mu = 0.8 \pm 0.05 \) (see supporting information section S1).

The sand flux is calculated from the hourly wind data of the weather station at Holloman Air Base (KHMN, 32°51′N, 106°06′W), using the method described in Courrech du Pont et al. (2014) (see also supporting information section S2). The wind is characterized by its shear velocity \( u_\ast \), representative of the logarithmic profile inside the turbulent boundary layer. Its threshold value \( u_{\text{th}} \) below which saltation cannot sustain steady transport is estimated with \( u_{\text{th}} = a \sqrt{(\rho_p/\rho_l)gd} = 0.35 \text{ m s}^{-1} \) and \( a = 0.1 \) (Iversen & Rasmussen, 1999). The corresponding typical velocity ratio \( u_\ast /u_{\text{th}} \) is then about 1.26 \( \pm 0.05 \) (all these values are gathered in Table S1). As shown in Figure 1a and documented by Pedersen et al. (2015), the wind regime

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Figure 1. The White Sands National Park dune field. (a) Satellite image of the White Sands Dune Field (Google™, Landsat-Copernicus). The left rose shows the wind data from 2007 to 2017 (direction toward which the wind is blowing). The right rose shows the corresponding distribution of sand flux orientations and the resultant flux direction (brown arrow). Both agree well with that reported by (Ewing et al., 2015; Pedersen et al., 2015). The blue area corresponds to the location of the digital elevation measurements. (b) Digital elevation data taken in June 2007. The dashed orange line is the location of the transect shown in (c), taken along the direction of the resultant flux. The red star is the location of the photo shown in (d), which is a view to the southwest of the dune field upwind margin.

Elevation data of the blue area in Figure 1a have been obtained using lidar-derived topography at five different times (June 2007, June 2008, January 2009, June 2010, and August 2015). Along the upwind margin, we observe that the sand transport is multimodal. Southwesterly winds dominate the transport as noted by the nearly unimodal sand flux distribution toward the northeast. The other modes from the north and southeast moderately impact the dune shape and migration (Swanson et al., 2016).
extracted 75 dune profiles from the surface elevation data, spaced 50 m apart and aligned with the direction of the resulting sand flux (Figure 1b). The average topography is removed using a Butterworth high-pass filter (order = 5, cutoff frequency = 0.005 m$^{-1}$). We limit our analysis to the first dunes of the filtered profile to ensure that we stay as much as possible in the early stage of dune growth (red area in Figure 1c). As shown by Figure 1d, these incipient dunes have very low aspect ratios and do not exhibit any slip faces (Phillips et al., 2019). The detrended bed elevation exhibits a spatially amplified oscillating behavior (Figures 2a and 2b). We now interpret these profiles using the theoretical framework provided by the linear stability analysis developed in the next section.

3. Dune Linear Stability Analysis

Here, we consider a unidirectional wind blowing at a constant shear velocity $u_\ast$, over a flat sedimentary bed. Above the transport threshold velocity $u_{th}$, the saturated sediment flux induced by this flow follows a quadratic law:

$$q_{sat} = \Omega \left( u_\ast^2 - u_{th}^2 \right),$$

where $\Omega$ is a dimensional constant that depends on fluid and grain properties (Creyssels et al., 2009; Durán et al., 2011; Iversen & Rasmussen, 1999; Ungar & Haff, 1987). In natural conditions, however, a sedimentary bed is never perfectly flat nor infinite, and these irregularities can be seen as the sum of different perturbations. The purpose of the linear stability analysis is precisely to study the temporal or spatial evolution of the bed in response to a perturbation of a given time or length scale. The emerging dune pattern is then expected to be dominated by the most unstable scale, associated with a sinusoidal mode of wavelength $\lambda$ and propagation velocity $c$, and whose amplitude grows in time with a rate $\sigma$ or in space over a length $\Lambda$. 

Figure 2. The spatial exponential dune growth. (a) Detrended profile corresponding to that of Figures 1b and 1c. The black dashed lines are exponential fits to the dune crests (black dots), giving $\Lambda = 225$ m (top) and $\Lambda = 135$ m (bottom). The theoretical red profile parameters are $C_0 = 0.06$ m, $\lambda = 120$ m, and $\Lambda = 170$ m. (b) Temporal evolution of the detrended elevation profile, with a close-up on one crest. (c) Schematics of the spatiotemporal dune development. The theoretical profile $h$ is defined in Equation 4.
Above such a sinusoidal bed, wind and sand flux are also modulated. As described in section 1, the basal shear stress is not in phase with the topography; this is quantified with two dimensionless coefficients, \( A \) and \( B \), which represent the in-phase and in-quadrature components, respectively. They are weak (logarithmic) functions of \( \lambda \) (Charru et al., 2013; Fourrière et al., 2010) but can be, in the first approximation for our purpose, considered as constant parameters of the model. The corresponding upwind shift of the wind with respect to the bed elevation is \( \sim \frac{\lambda A}{2\pi} \). Similarly, the actual sediment flux \( q \) is not saturated but delayed with respect to the basal shear stress, a process quantified by the saturation length \( L_{\text{sat}} \). These are the main physical mechanisms of the dune formation model from which the stability analysis is derived (see supporting information section S3 for the proper technical derivation and related theoretical figures).

Consider first a large flat extent of sand. Under the action of the wind, dunes emerge everywhere simultaneously: There is no spatial development of the pattern. A spatial sinusoidal perturbation characterized by a given wavelength \( \lambda \) and an initial amplitude \( C_0 \) can grow or decay in time, at a rate \( \sigma \), in response to the wind shift and the flux lag. The perturbation also propagates at a velocity \( c \). The bed elevation along the direction \( x \) of the wind can be written as follows:

\[
 h(x, t) = C_0 e^{\sigma t} \cos \left[ \frac{2\pi}{\lambda} (x - ct) \right].
\]  

(3)

Both temporal growth rate and propagation speed can be computed as functions of \( \lambda \) from the analysis of the equations coupling the flow, sediment transport, and bed evolution, constituting the dispersion relation of sand waves (supporting information section S3). Positive values of the growth rate are associated with unstable perturbations, and these are typically for large values of \( \lambda \). Conversely, small wavelengths are stable, with \( \sigma < 0 \).

Consider now a sediment bed bounded upwind such that disturbances cannot grow at a specific position in space, noted here \( x = 0 \). Dunes emerge from the selective amplification of disturbances propagating downwind from the field entrance. This results in a spatial development of the pattern. There is no temporal growth: At a given location, the amplitude of the bed oscillation is the same at any time. The form of a sinusoidal mode of initial amplitude \( C_0 \) can be written as follows:

\[
 h(x, t) = C_0 e^{i\lambda x} \cos \left[ \frac{2\pi}{\lambda} (x - ct) \right],
\]  

(4)

where \( \Lambda^{-1} \) is the spatial growth rate of the dunes.

Neutral modes are the same in both spatial and temporal analyses. Their wavelength \( \lambda_c \) is characterized by vanishing growth rates \( \sigma (\lambda_c) = 0 \) and \( \Lambda^{-1} (\lambda_c) = 0 \), such that

\[
 \lambda_c = \frac{2\pi A}{B - \frac{1}{\mu} \left( \frac{u_{th}}{u_*} \right)^2 L_{\text{sat}}},
\]  

(5)

and separates growing \( (\lambda > \lambda_c) \) from decaying \( (\lambda < \lambda_c) \) perturbations. It can thus be interpreted as a minimal dune size.

Performing the temporal linear stability analysis (denoted by subscript T), in the limit \( L_{\text{sat}}/\lambda_c \ll 1 \), the characteristics of the fastest growing perturbation read

\[
 \lambda_T \sim \frac{3}{2} \lambda_c,
\]  

(6)

\[
 \sigma_T \sim \frac{Q}{L_{\text{sat}}^2} \frac{A}{2} \left( \frac{2\pi L_{\text{sat}}}{\lambda_T} \right)^3,
\]  

(7)

\[
 c_T \sim \frac{Q}{L_{\text{sat}}} \frac{A}{2} \frac{2\pi L_{\text{sat}}}{\lambda_T}.
\]  

(8)

where \( Q = \Omega u_*^2 \) gives the characteristic scale of the sediment flux associated with the wind regime (Fourrière et al., 2010; Gadal et al., 2019).
Conversely, spatial growth rate reaches a maximum $1/\Lambda_S$ at some specific value of the wavelength, noted $\lambda_S$, corresponding to the propagation velocity $c_S$. Unfortunately, no simple analytical and accurate formulae like (6)–(8) can be derived for these quantities (see supporting information section S3). Temporal and spatial analyses are consistent, and we typically find $\lambda_S \approx 1.3 \lambda_T$ and $c_S \approx 0.77 c_T$. The numerical factors in these relations do not vary by more than a few percent upon changing the parameters $A$ and $B$ within a reasonable range of values. In the spatial development of the instability, an individual bump grows in height while propagating downwind at a constant velocity. Its amplitude therefore varies exponentially with respect to time, and one can define a temporal growth rate $\zeta_S \equiv c_S/\lambda_S$ (inset of Figure 2c) in the frame of reference of the bump, that is, a Lagrangian growth rate. The theoretical analysis provides the approximate relation $\zeta_S \approx 0.43 \sigma_T$. Both $\zeta_S$ and $\Lambda_S$ can be measured from the field data, providing equivalent information.

4. Field Data Analysis

After removing the average topography (Figure 1c), the detrended bed elevation profile exhibits an exponentially amplifying sinusoidal shape, as predicted by the spatial linear theory for dune emergence (Figure 2a). Using these profiles and their temporal evolution (Figure 2b), we have extracted the three independent characteristics of the pattern ($\lambda$, $c$, and $\Lambda$ or $\zeta$) using two different methods. For each profile, we either look at each peak separately (peak-to-peak method) or extract quantities averaged over the whole profile (global approach).

The wavelength $\lambda$ is computed by autocorrelation of the bed elevation profile (global method) and from the spacing between two adjacent peaks (peak-to-peak method). The fit of an exponential to the peaks of each profile gives the spatial growth length $\Lambda$ (global method, see dashed line in Figure 2a). The spatial growth length is alternatively computed from the difference in height between two adjacent peaks (peak-to-peak method, see Figure 2c).

The Lagrangian growth rate $\zeta$ and propagation velocity $c$ are obtained by fitting exponential and linear functions to the temporal variation of the dune height and position, respectively (see Equations S43 and S44). The peak-to-peak method looks at the height and position of each peak separately (see inset of Figure 2c). For a global measurement, the average propagation speed can be determined from the cross-correlation curve between the same profiles at different times and the average Lagrangian growth rate from the temporal evolution of the bed elevation standard deviation.

Importantly, to extract the average values of $\zeta$ and $c$, we take into account the temporal variations of the characteristic sand flux $Q$. Indeed, both quantities vary in time proportionally to $Q$. We also remove periods of time when the wind is below the transport threshold (see supporting information section S4).

5. Time and Length Scales of the Incipient Dunes

The output of the analysis of the 75 transects is shown in Figure 3. Both peak-to-peak and global methods exhibit similar distributions for the wavelength $\lambda$, the propagation velocity $c$, the Lagrangian growth rate $\zeta$, and the growth length $\Lambda$, with clear dominant (most probable) values. The incipient dune wavelength and growth length are both on the order of a hundred meters; their propagation velocity is around 5 m year$^{-1}$, and their growth rate is about 0.015 year$^{-1}$. These values, as well as the typical dispersion around them (i.e., the width of these distributions), are more precisely reported in Table S2. For $\lambda$ and $c$, our results are consistent with the measurements of Phillips et al. (2019), made on a single elevation profile. Their dispersion is on the order of 20%, because these quantities can be measured with a good accuracy, especially with the global method using correlation. As the measurement of $\Lambda$ and $\zeta$ is more delicate, the corresponding distributions are more dispersed. The peak-to-peak method is actually sensitive to the behavior of individual peaks, which can respond to various types of local disturbances. For example, they may induce irregularities in the spacing between the peaks, or asymmetry between positive and negative detrended topography (Figure 2b). As a result, a few negative values of the velocity, growth rate, and characteristic growth length are reported. Nevertheless, these data provide reliable and meaningful statistics to test the theory, which must be able to account for those four quantities concomitantly. The free parameters of the linear analysis are the hydrodynamic coefficients $A$ and $B$, as the others are set independently with the wind and sediment properties (see Table S1).
The incipient dune wavelength peaks around 120 m and is therefore significantly larger than the usually reported value ($\approx 20$ m, for sand particles of size $180 \mu m$) (Elbelrhiti et al., 2005). How can the theory reproduce such a large value? First, as the wavelength is proportional to the saturation length and thus to the grain size (Equations 1, 5, and 6), the presence here of much coarser grains provides a factor $670/180 \approx 3.7$ corresponding to the ratio of grain diameter. Second, the most unstable wavelength is predicted to increase when sediment transport occurs close to the threshold, in relation to the denominator of Equation 5 (Andreotti et al., 2010; Charru et al., 2013; Gadal et al., 2019). Here, with $u^*/u_{th} \approx 1.3$, we can expect an additional factor of 2 with respect to a situation far above threshold. The simultaneous fit of the four quantities predicted by the spatial linear stability analysis to the data allows us to reproduce quantitatively the dominant wavelength and growth rate. The predicted values fall in the peak of the distributions (red lines in Figures 3a and 3c). This adjustment, however, overestimates the growth length and the propagation velocity, whose predictions exceed the dominant values by an amount comparable to the peaks’ width (red lines in Figures 3b and 3d).

This discrepancy can be understood by questioning our approximation of a unidirectional wind. A finer analysis of the flux rose shows in fact secondary winds, with nonzero components perpendicular to the crest toward the southwest. Reversing winds have cumulative effects on the growth rate and the selected wavelength. They, however, partially cancel each other out, impeding the propagation and thus the spatial development of the dune pattern. Such a process is supported by observations of reactivation surfaces formed by reversing winds in the stratigraphy at White Sands (Kocurek et al., 2007; Phillips et al., 2019). The value of the characteristic sand flux $Q$ (given in Table S1) is a time average that does not account for changes in wind orientation. The ratio between the scalar and vector averages of $Q$, taking into account the variations in orientation of the sand fluxes over time, is about 0.6 (see supporting information section S4). Once corrected by this ratio, the predicted migration velocity and growth length come into quantitative agreement with the corresponding dominant values of the distributions (orange lines in Figure 3).

**Figure 3.** Distributions of incipient dune time and length scales. Blue and green distributions show the results of the global and peak-to-peak methods, respectively. Error bars give the range of values obtained from the spatial linear stability analysis with $\lambda = 3.6 \pm 0.6$ and $B = 1.9 \pm 0.3$, and dots show the average. Raw predictions based on a unidirectional wind are in red, and predictions taking into account the correction due to reversing winds are in orange (see Table S2). The cutoff wavelength $\lambda_c$ is in gray.
6. Discussion

The exponentially amplified sinusoidal behavior of the White Sands bed elevation profiles is field evidence for the spatial development of the dune instability. The linear analysis is able to quantitatively reproduce the three characteristics of the emergent pattern: dune wavelength, propagation velocity, and growth length (or equivalently, growth rate). To obtain this agreement, the two hydrodynamic coefficients where adjusted, resulting in $A = 3.6 \pm 0.6$ and $B = 1.9 \pm 0.3$. All the other parameters of the theory were fixed independently from sediment and wind data, either by direct measurement (grain diameter and density, and avalanche slope) or using well-calibrated relationships (saturation length and sediment flux). Note that the uncertainty on the determined coefficients is dominated by the those of the fixed parameters rather than by the dispersion in the measurements of $c$, $\lambda$, and $\Lambda$. Overall, the value of $L_{\text{sat}}$, involved in $\lambda$ and $\Lambda$, directly affects the estimate of $B/A$, while the value of $Q$, involved in $c$, mostly affects $A$.

Importantly, the concomitant agreement of $c$, $\lambda$, and $\Lambda$ is a stringent test of the theory. This study is therefore a step forward in the general “dune inverse problem,” trying to infer, for example, grain or wind properties from dune characteristics (Ewing et al., 2015; Fenton, Michaels, & Beyer, 2014; Fenton, Michaels, Chojnacki, & Beyer, 2014; Fernandez-Cascales et al., 2018; Runyon et al., 2017). It is remarkable that the resulting values determined from our field data are very close to those directly measured by Claudin et al. (2013) on a single 40-m-long dune ($A \approx 3.4$ and $B \approx 1.6$), as well as to the predictions of hydrodynamic models (Charru et al., 2013; Fourrière et al., 2010). This study thus confirms the reliability of the linear analysis in the interpretation of field, experimental, or numerical data relating to the emergence of incipient dunes (Elbelrhiti et al., 2005; Fourrière et al., 2010; Gadal et al., 2019; Narteau et al., 2009).

A limitation of the linear theory is of course the presence of nonlinear effects. They occur when the aspect ratio of the sand waves becomes too large or when the dunes interact with each other, so that each bed perturbation cannot be considered as independent of the others. Bumps with aspect ratios above $\approx 1/13$ are expected to start to develop flow recirculation on their downwind side, usually associated with the formation of an avalanche slip face (Fourrière et al., 2010). In the region we have studied, the waves furthest inside the dune field could reach aspect ratios of about 1/10, but no slip faces were observed. Similar to Phillips et al. (2019), we also recognize the coexistence of multiple wavelengths at the upwind side of the profiles (associated with different celerities and growth rates or lengths), and these are partly the cause of the distribution widths in Figure 3. We could not, however, infer from these data signs of interactions, such as collisions, coalescence or ejection (Bacik et al., 2020; Gao et al., 2015; Hersen & Douady, 2005; Katsuki et al., 2005).

Although studied here at the boundary of a dune field, the spatial development of the dune instability is also present on preexisting large dunes, providing a similar upwind boundary condition in terms of sand availability. As a matter of fact, the emergence of bed oscillations on the flanks of barchans has been proposed as a key mechanism to understand their stability, as these superimposed waves eventually grow until they can break from the horns, causing large sand losses (Elbelrhiti et al., 2005; Lee et al., 2019; Zhang et al., 2010). Likewise, in narrow bidirectional wind regimes, the growth of the instability over elongating linear dunes breaks them into trains of barchans (Gao et al., 2015). This work therefore provides a reliable base to study the stability of large dunes and thus the formation of large-scale structures inside dune fields (Gadal et al., 2020; Worman et al., 2013).

Data Availability Statement

Meteorological data used in this manuscript are hosted by MesoWest under the station code “KHNM” (https://mesowest.utah.edu/cgi-bin/droman/mesomap.cgi?state=NM&rawsflag=3). Topographic data can be found in the public repositories Texas Data Repository and OpenTopography (2007: https://doi.org/10.18738/T8/WUNFOG, 2008: https://doi.org/10.18738/T8/HQVSX, 2009: https://doi.org/10.5069/G9Q23XSP, 2010: https://doi.org/10.5069/G97D2S2D, and 2015: https://portal.opentopography.org/usgsDataset?dsid=USGS_LPC_NM_WhiteSands_2015_LAS_2017). Supporting information figures, tables, and text can be found in the supporting information.
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