Missing Value Prediction for Qualitative Information Systems

T. Medhat\textsuperscript{a}, Manal Elsayed\textsuperscript{b}

\textsuperscript{a}Electrical Engineering Department, Faculty of Engineering, Kafrelsheikh University, Kafrelsheikh, Egypt
\textsuperscript{b}Physics and Engineering Mathematics Department, Faculty of Engineering, Kafrelsheikh University, Kafrelsheikh, Egypt

Abstract. Most information systems usually have some missing values due to unavailable data. Missing values have a negative impact on the quality of classification rules generated by data mining systems. They make it difficult to obtain useful information from the data set. Solving the missing data problem is a high priority in the fields of knowledge discovery and data mining. The main goal of this paper is to suggest a method for converting a qualitative information system into a binary system, by using a distance function between condition attributes, we can detect the missing values for decision attribute according to the smallest distance. Most common values can be used to solve the problem of repeated small distance for some cases. This method will be discussed in detail through a case study.

1. Introduction

Missing data is the situation where some values of some cases are missing. Dealing with missing data \cite{9,10,14,16,17} is time-consuming. In our experience, fixing up problems caused by missing data sometimes takes longer than the analysis itself. Missing data or more generally incomplete data \cite{1} (e.g. censored data which are partially missing because we know which intervals they fall into) occur frequently in medical studies, in the forms of nonresponse in patient surveys, noncompliance in clinical trials, nonreporting or delayed reporting to health surveillance systems, just to list a few. Three major difficulties with such incomplete-data problems are: (I) loss of information, efficiency or power due to loss of data; (II) complication in data handling, computation and analysis due to irregularities in the data patterns and nonapplicability of standard software and (III) potentially very serious bias due to systematic differences between the observed data and the unobserved data.

The best way of dealing with these problems, of course, is to avoid them in the first place. Unfortunately, in most real-life studies, be they medical or otherwise, the problem of incomplete data is unavoidable even if we have made the greatest possible efforts \cite{1}. There are three different methods for imputing missing data as described in \cite{3}. Similarity measure is fundamental to many machine learning and data mining; similarity is learned from the data, so it will be more unbiased than that measured by traditional similarity metrics \cite{6}. In the real-world applications, heterogeneous interdependent attributes that consist of both discrete and numerical variables can be observed ubiquitously \cite{15}.
In many predictive modeling applications, useful attribute values ("features") may be missing. For example, patient data often have missing diagnostic tests that would be helpful for estimating the likelihood of diagnoses or for predicting treatment effectiveness. Consumer data often do not include values for all attributes useful for predicting buying preferences. It is important to distinguish two contexts: features may be missing at induction time, in the historical “training” data, or at prediction time, in to-be-predicted “test” cases. This paper introduces techniques for handling missing values at prediction time. Research on missing data in machine learning and statistics has been concerned primarily with induction time. Much less attention has been devoted to the development and to the evaluation of policies for dealing with missing attribute values at prediction time. Importantly for anyone wishing to apply models such as classification trees, there are almost no comparisons of existing approaches nor analyses or discussions of the conditions under which the different approaches perform well or poorly [13]. Rough Set Theory, proposed in 1982 by Zdzislaw Pawlak, is in a state of constant development. Its methodology is concerned with the classification and analysis of imprecise, uncertain or incomplete information and knowledge, and it is considered one of the first non-statistical approaches in data analysis [11, 12]. The fundamental concept behind Rough Set Theory is the approximation of lower and upper spaces of a set, the approximation of spaces being the formal classification of knowledge regarding the interesting domain [8]. The subset generated by lower approximations is characterized by objects that will definitely form part of an interesting subset, whereas the upper approximation is characterized by objects that will possibly form part of an interesting subset. Every subset defined through upper and lower approximation is known as Rough Set. Over the years Rough Set Theory has become a valuable tool in the resolution of various problems, such as: representation of uncertain or imprecise knowledge; knowledge analysis; evaluation of quality and availability of information with respect to consistency; identification and evaluation of data dependency; reasoning based on uncertain and reduct of information data. The extent of rough set applications used today is much wider than in the past, principally in the areas of medicine, analysis of database attributes and process control. In this paper, we use the concepts of Rough Sets for attribute reduction [2, 4]. Many methods are sensitive to the used distance metric [5, 7]. The proposed method heavily depends on distance, and that is not sensitive to use the distance metric, because we calculate the distance after converting the system into binary system. Therefore, the result of distances belongs to the limited set of values: \{0, 1, \sqrt{2}, \sqrt{3}, \sqrt{4}, \ldots, \sqrt{N}\} where N is the number of condition attributes.

In this paper, we begin with section 2 as an introduction to the basic concepts. Section 3 introduces the method of converting qualitative information system into the binary information system. Section 4 introduces the method of missing values prediction, and at the last section, we conclude this paper.

2. Basic Concepts

2.1. Information System:

Let IS = (U, A ∪{d}) be an information system, where U is the universe with a non-empty set of finite objects. A is a nonempty finite set of condition attributes, and d is the decision attribute (such a table is also called decision table). ∀a ∈ A there is a corresponding function f_a : U → V_a, where V_a is the set of values of a. If P ⊆ A, there is an associated equivalence relation [8, 11, 12]: as shown in Table 1.

| U/A Condition attributes | Decision attribute |
|--------------------------|-------------------|
| a | b | c | D |
| **O1** | 1 | 1 | 5 | accept |
| **O2** | 2 | 0 | 3 | reject |
| **O3** | 1 | 0 | 3 | reject |
| **O4** | 2 | 0 | 4 | accept |

Table 1: Example of information system table
2.2. Qualitative information system:

If some values of condition attributes are non-numerical values, then that information system is called qualitative information system as shown in Table 2.

Table 2: Example of qualitative information system table

| U/A | Condition attributes | Decision attribute |
|-----|----------------------|--------------------|
|     | a       | b   | c  | D   |
| x1  | 1       | high| yes| yes |
| x2  | 2       | low | no  | no  |
| x3  | 1       | low | no  | no  |
| x4  | 2       | medium | yes | yes |

2.3. Binary information system:

If all values of condition attributes are binary values (0 or 1), then that information system is called binary information system as shown in Table 3.

Table 3: Example of binary information system table

| U/A | Condition attributes | Decision attribute |
|-----|----------------------|--------------------|
|     | a  | b  | c  | D   |
| 1   | 1  | 1  | 0  | yes |
| 2   | 0  | 1  | 1  | yes |
| 3   | 0  | 0  | 0  | no  |
| 4   | 1  | 0  | 1  | yes |

2.4. Reduction of Condition Attributes Relative to Decision Attribute

Definition 2.1.
If C and D are the condition and decision attributes respectively. Then relative discernibility matrix [11] is:

\[ M^D_C(x, y) = \{a \in C : a(x) \neq a(y), D(x) \neq D(y)\} \]

Definition 2.2.
If C and D are the condition and decision attributes respectively. Then relative discernibility function [11] is:

\[ f^D_C = \land\{\forall a : a \in M^D_C \neq \emptyset\} \]

which is used for reduction of condition attributes relative to decision attribute.

2.5. Missing values:

If some values of decision attribute have quotation mark “?” as a value, then this value is called missing value, and we need to detect the values of missing values according to the given information system.
2.6. Distance function:

The distance between objects according to the values of condition attributes, can be calculated by the following function:

$$\text{dis}(O_i, O_j) = \sqrt{\sum_{k=1}^{N} [c_k(O_i) - c_k(O_j)]^2}$$

where $O_i, O_j \in U, c_k \in C, N = |C| = \text{number of condition attributes}$

2.7. The most common value:

The value of decision attribute which is repeated more than others, which is congruent to the statistical concept mode.

3. Converting into Binary System

In the following examples, by converting each column of condition attribute into a number of columns equal to the number of its different values. If its value exists ”it takes 1” else ”it takes 0”. If the value of an attribute is only two values, then we put it as a single column ”one of its value takes 1 and other takes 0” instead of increasing the columns without any usefulness. If the value of an attribute is only one value, we delete its column. See the following figure:

3.1. Conversion rules:

The conversion rules according to the types of information system are shown in Figure 1 as follows:

1. If an attribute has one value → We delete this attribute.
2. If an attribute has two different values → We convert its values one of them takes ”0” and the other takes ”1”.
3. If an attribute has three different values → We convert it into three attributes (columns), takes values ”0” or ”1”, according to the position of values.

Figure 1: Example of converting into Binary system
4. Prediction of missing values

We will introduce a method (depending on the reduction of attributes, distance function, and most common values) to predict the decision for missing values. This will be done by:

1. Convert qualitative information system into a binary system.
2. Divide the binary information table into two tables, one of them is complete and the other is incomplete.
3. If needed, make a reduction of attributes for the complete decision table.
4. Compute the distance metric between objects of complete table and incomplete table.
5. The smallest distance means that the decision for missing value of the incomplete decision table equals the decision value of the complete decision table of the complete object which makes that distance.
6. If the small distance is repeated with more than one object, then we use the method of most common values, where we select the decision which has the largest number of repetition with the complete decision table.

See the following example.

Example:
The optometrist’s data collection concerns the optician’s decision as to whether or not the patient is suitable for contact lenses. The set of all possible decisions is listed in Table 4, which has 6 missing values “?” of the decision.

Where \( U = \{P1, P2, \ldots, P24\} \), \( A = \{age, Spectacle, Astigmatic, Tear production rate\} \), and \( D = \{Optician’s decision\} \)

EXPERIMENTAL RESULTS:

1) Converting the qualitative information system into a binary system, we get to Table 5:
2) Dividing the binary system into complete decision table and incomplete decision table as shown in Table 6 and Table 7.

3) Making a reduction of condition attributes relative to decision attribute of the complete decision table, which give us the following reducts:
   Reducts: \{[b, c, d, g, h], [b, c, d, g, i], [a, c, e, f, i], [b, c, f, i], [a, b, e, g, i], [a, b, d, g, i], [a, b, e, f, h], [b, c, e, f, h], [a, b, d, g, h], [a, c, d, g, h], [a, c, d, f, i], [a, b, e, g, h], [b, c, e, f, i], [b, c, e, g, h], [a, c, e, f, h], [a, c, e, g, h], [b, c, e, g, i], [a, c, d, g, i], [a, b, d, f, h], [b, c, d, f, h], [a, c, e, g, i], [a, b, d, f, i]\}
   We select one of them, which gives Table 8 and Table 9.

4) Calculating the distance function between the objects of incomplete decision table and complete decision table after reduction of condition attributes:

From Table 10, we find that:
The decision of object P13 \( \Rightarrow \) will be “no contact lenses”.
The decision of object P14 \( \Rightarrow \) will be “soft contact lenses”.
The decision of object P19 \( \Rightarrow \) will be “no contact lenses”.
And the decision of object P20 \( \Rightarrow \) will be “hard contact lenses”.
But we can’t predict the missing values of objects P1, and P7, according to the repetition of small distance with more than one object which has different decisions. So we need to calculate the most common values of decision values.

5) Calculating the most common values for all values of decision attribute, and applying this method to detect the missing values for repeated small distance, as shown in Table 11.
Table 4: The optician’s decisions data set

| U/A | Condition attributes | Decision attribute (Optician’s decision) |
|-----|----------------------|------------------------------------------|
|     | Age                  | Spectacle | Astigmatic | Tear production rate |                               |
| P1  | Young                | Hypermetropia | No | Reduced | ?                     |
| P2  | Young                | Hypermetropia | No | Normal  | soft contact lenses  |
| P3  | Pre-presbyopic       | Hypermetropia | No | Reduced | no contact lenses    |
| P4  | Pre-presbyopic       | Hypermetropia | No | Normal  | soft contact lenses  |
| P5  | Presbyopic           | Hypermetropia | No | Reduced | no contact lenses    |
| P6  | Presbyopic           | Hypermetropia | No | Normal  | soft contact lenses  |
| P7  | Young                | Hypermetropia | Yes | Reduced | ?                     |
| P8  | Young                | Hypermetropia | Yes | Normal  | hard contact lenses  |
| P9  | Pre-presbyopic       | Hypermetropia | Yes | Reduced | no contact lenses    |
| P10 | Pre-presbyopic       | Hypermetropia | Yes | Normal  | no contact lenses    |
| P11 | Presbyopic           | Hypermetropia | Yes | Reduced | no contact lenses    |
| P12 | Presbyopic           | Hypermetropia | Yes | Normal  | no contact lenses    |
| P13 | Young                | Myope      | No   | Reduced | ?                     |
| P14 | Young                | Myope      | No   | Normal  | ?                     |
| P15 | Pre-presbyopic       | Myope      | No   | Reduced | no contact lenses    |
| P16 | Pre-presbyopic       | Myope      | No   | Normal  | soft contact lenses  |
| P17 | Presbyopic           | Myope      | No   | Reduced | no contact lenses    |
| P18 | Presbyopic           | Myope      | No   | Normal  | no contact lenses    |
| P19 | Young                | Myope      | Yes  | Reduced | ?                     |
| P20 | Young                | Myope      | Yes  | Normal  | ?                     |
| P21 | Pre-presbyopic       | Myope      | Yes  | Reduced | no contact lenses    |
| P22 | Pre-presbyopic       | Myope      | Yes  | Normal  | hard contact lenses  |
| P23 | Presbyopic           | Myope      | Yes  | Reduced | no contact lenses    |
| P24 | Presbyopic           | Myope      | Yes  | Normal  | hard contact lenses  |

Table 12 shows the prediction of missing values of objects P1 and P7 after computing the most common values of decision attribute.
Table 5: The optician’s decisions data set after converting to a binary system

| U/A | Age | Spectacle | Astigmatic | Tear production rate | Decision |
|-----|-----|-----------|------------|----------------------|----------|
|     | Young | Pre-presbyopic | Presbyopic | Hypermetropia | Myope | No | Yes | Reduced | Normal |
| P1  | 1    | 0          | 0          | 1         | 0  | 1  | 0  | 1  | 0  | ?     |
| P2  | 1    | 0          | 0          | 1         | 0  | 0  | 1  |    |    | soft contact lenses |
| P3  | 0    | 1          | 0          | 0         | 0  | 1  | 0  |    |    | no contact lenses   |
| P4  | 0    | 1          | 0          | 1         | 0  | 0  | 1  |    |    | soft contact lenses |
| P5  | 0    | 0          | 1          | 1         | 0  | 1  | 0  |    |    | no contact lenses   |
| P6  | 0    | 0          | 1          | 1         | 0  | 0  | 1  |    |    | soft contact lenses |
| P7  | 1    | 0          | 0          | 1         | 0  | 0  | 1  | 1  | 0  | ?     |
| P8  | 1    | 0          | 0          | 1         | 0  | 0  | 1  |    |    | hard contact lenses |
| P9  | 0    | 1          | 0          | 1         | 0  | 1  | 0  |    |    | no contact lenses   |
| P10 | 0    | 1          | 0          | 1         | 0  | 0  | 1  |    |    | no contact lenses   |
| P11 | 0    | 0          | 1          | 1         | 0  | 1  | 0  |    |    | no contact lenses   |
| P12 | 0    | 0          | 1          | 0         | 0  | 1  | 0  |    |    | no contact lenses   |
| P13 | 1    | 0          | 0          | 0         | 1  | 1  | 0  | 1  | 0  | ?     |
| P14 | 1    | 0          | 0          | 0         | 1  | 1  | 0  | 0  | 1  | ?     |
| P15 | 0    | 1          | 0          | 0         | 1  | 1  | 0  | 1  | 0  | no contact lenses   |
| P16 | 0    | 1          | 0          | 0         | 1  | 1  | 0  | 0  | 1  | soft contact lenses |
| P17 | 0    | 0          | 1          | 0         | 1  | 0  | 1  |    |    | no contact lenses   |
| P18 | 0    | 0          | 1          | 0         | 1  | 0  | 0  |    |    | no contact lenses   |
| P19 | 1    | 0          | 0          | 0         | 1  | 0  | 1  | 0  |    | ?     |
| P20 | 1    | 0          | 0          | 0         | 1  | 0  | 1  |    |    | ?     |
| P21 | 0    | 1          | 0          | 0         | 1  | 1  | 0  |    |    | no contact lenses   |
| P22 | 0    | 1          | 0          | 0         | 1  | 0  | 1  |    |    | hard contact lenses |
| P23 | 0    | 0          | 1          | 0         | 1  | 1  | 0  |    |    | no contact lenses   |
| P24 | 0    | 0          | 1          | 0         | 1  | 0  | 1  |    |    | hard contact lenses |
### Table 6: Complete decision table

| # | U/A | Age | Spectacle | Astigmatic | Tear production rate | D       |
|---|-----|-----|-----------|------------|----------------------|---------|
|   |     |     | Young     | Pre-presbyopic | Presbyopic | Hypermetropia | Myope | No | Yes | Reduced | Normal | Decision |
| 1 | P2  | 1   | 0         | 0           | 1         | 0       | 1     | 0  | 0  | 1       |         | soft contact lenses |
| 2 | P3  | 0   | 1         | 0           | 1         | 0       | 1     | 0  | 1  | 0       |         | no contact lenses   |
| 3 | P4  | 0   | 1         | 0           | 1         | 0       | 1     | 0  | 0  | 1       |         | soft contact lenses |
| 4 | P5  | 0   | 0         | 1           | 1         | 0       | 1     | 0  | 1  | 0       |         | no contact lenses   |
| 5 | P6  | 0   | 0         | 1           | 1         | 0       | 1     | 0  | 0  | 1       |         | soft contact lenses |
| 6 | P8  | 1   | 0         | 0           | 1         | 0       | 0     | 1  | 0  | 1       |         | hard contact lenses |
| 7 | P9  | 0   | 1         | 0           | 1         | 0       | 0     | 1  | 1  | 0       |         | no contact lenses   |
| 8 | P10 | 0   | 1         | 0           | 1         | 0       | 0     | 1  | 0  | 1       |         | no contact lenses   |
| 9 | P11 | 0   | 0         | 1           | 1         | 0       | 0     | 1  | 1  | 0       |         | no contact lenses   |
|10 | P12 | 0   | 0         | 1           | 1         | 0       | 0     | 1  | 0  | 1       |         | no contact lenses   |
|11 | P13 | 0   | 1         | 0           | 0         | 1       | 1     | 0  | 1  | 0       |         | no contact lenses   |
|12 | P14 | 0   | 1         | 0           | 0         | 1       | 1     | 0  | 0  | 1       |         | soft contact lenses |
|13 | P15 | 0   | 0         | 1           | 0         | 1       | 0     | 1  | 0  | 1       |         | no contact lenses   |
|14 | P16 | 0   | 0         | 1           | 0         | 1       | 0     | 1  | 0  | 1       |         | no contact lenses   |
|15 | P17 | 0   | 0         | 1           | 0         | 1       | 0     | 1  | 0  | 1       |         | no contact lenses   |
|16 | P18 | 0   | 0         | 1           | 0         | 1       | 0     | 0  | 1  | 0       |         | no contact lenses   |
|17 | P19 | 0   | 0         | 0           | 1         | 0       | 1     | 1  | 0  | 1       |         | no contact lenses   |
|18 | P20 | 0   | 0         | 1           | 0         | 1       | 0     | 1  | 0  | 1       |         | hard contact lenses |

### Table 7: Incomplete decision table

| # | U/A | Age | Spectacle | Astigmatic | Tear production rate | D       |
|---|-----|-----|-----------|------------|----------------------|---------|
|   |     |     | Young     | Pre-presbyopic | Presbyopic | Hypermetropia | Myope | No | Yes | Reduced | Normal | Decision |
| 1 | P1  | 1   | 0         | 0           | 1         | 0       | 1     | 0  | 1  | 0       |         | ?        |
| 2 | P7  | 1   | 0         | 0           | 1         | 0       | 0     | 1  | 1  | 0       |         | ?        |
| 3 | P13 | 1   | 0         | 0           | 0         | 1       | 1     | 0  | 1  | 0       |         | ?        |
| 4 | P14 | 1   | 0         | 0           | 0         | 1       | 1     | 0  | 0  | 1       |         | ?        |
| 5 | P19 | 1   | 0         | 0           | 0         | 1       | 0     | 1  | 1  | 0       |         | ?        |
| 6 | P20 | 1   | 0         | 0           | 0         | 1       | 0     | 1  | 0  | 1       |         | ?        |
Table 8: Complete decision table after reduction

| #  | U/A | Age (Young) | Age (Presbyopic) | Spectacle (Hypermetropia) | Astigmatic (No) | Tear production rate (Reduced) | Decision         |
|----|-----|-------------|------------------|---------------------------|-----------------|---------------------------------|------------------|
| 1  | P2  | 1           | 0                | 1                         | 1               | 0                               | soft contact lenses |
| 2  | P3  | 0           | 0                | 1                         | 1               | 1                               | no contact lenses |
| 3  | P4  | 0           | 0                | 1                         | 1               | 0                               | soft contact lenses |
| 4  | P5  | 0           | 1                | 1                         | 1               | 1                               | no contact lenses |
| 5  | P6  | 0           | 1                | 1                         | 1               | 0                               | soft contact lenses |
| 6  | P8  | 1           | 0                | 1                         | 0               | 0                               | hard contact lenses |
| 7  | P9  | 0           | 0                | 1                         | 0               | 1                               | no contact lenses |
| 8  | P10 | 0           | 0                | 1                         | 0               | 0                               | no contact lenses |
| 9  | P11 | 0           | 1                | 1                         | 0               | 1                               | no contact lenses |
| 10 | P12 | 0           | 1                | 1                         | 0               | 0                               | no contact lenses |
| 11 | P15 | 0           | 0                | 0                         | 1               | 1                               | no contact lenses |
| 12 | P16 | 0           | 0                | 0                         | 1               | 0                               | soft contact lenses |
| 13 | P17 | 0           | 1                | 0                         | 1               | 1                               | no contact lenses |
| 14 | P18 | 0           | 1                | 0                         | 1               | 0                               | no contact lenses |
| 15 | P20 | 0           | 0                | 0                         | 0               | 1                               | no contact lenses |
| 16 | P22 | 0           | 0                | 0                         | 0               | 0                               | hard contact lenses |
| 17 | P23 | 0           | 1                | 0                         | 0               | 1                               | no contact lenses |
| 18 | P24 | 0           | 1                | 0                         | 0               | 0                               | hard contact lenses |

Table 9: Incomplete decision table after reduction

| #  | U/A | Age (Young) | Age (Presbyopic) | Spectacle (Hypermetropia) | Astigmatic (No) | Tear production rate (Reduced) | Decision         |
|----|-----|-------------|------------------|---------------------------|-----------------|---------------------------------|------------------|
| 1  | P1  | 1           | 0                | 1                         | 1               | 1                               | ?                |
| 2  | P7  | 1           | 0                | 1                         | 0               | 1                               | ?                |
| 3  | P13 | 1           | 0                | 0                         | 1               | 1                               | ?                |
| 4  | P14 | 1           | 0                | 0                         | 1               | 0                               | ?                |
| 5  | P19 | 1           | 0                | 0                         | 0               | 1                               | ?                |
| 6  | P20 | 1           | 0                | 0                         | 0               | 0                               | ?                |
Table 10: Decision Table of Missing Values of Some Objects

| Objects with missing decision | Objects with decision | Small distance | Decision of complete objects | Decision of incomplete objects |
|-------------------------------|----------------------|----------------|------------------------------|-------------------------------|
| P1                            | P2                   | 1              | soft contact lenses         | ?                             |
|                               | P3                   | 1              | no contact lenses           | ?                             |
| P7                            | P8                   | 1              | hard contact lenses         | ?                             |
|                               | P9                   | 1              | no contact lenses           | ?                             |
| P13                           | P15                  | 1              | no contact lenses           | no contact lenses             |
| P14                           | P2                   | 1              | soft contact lenses         | soft contact lenses           |
|                               | P16                  | 1              | soft contact lenses         |                              |
| P19                           | P21                  | 1              | no contact lenses           | no contact lenses             |
| P20                           | P8                   | 1              | hard contact lenses         | hard contact lenses           |
|                               | P22                  | 1              | hard contact lenses         |                              |

Table 11: The most common values of decision values

| Decision values | Number of repetition |
|-----------------|----------------------|
| no contact lenses | 11                   |
| soft contact lenses | 4                   |
| hard contact lenses | 3                   |

Table 12: Decision Table of Missing Values of P1 and P7

| Objects with missing decision | Objects with decision | Small distance | Decision of complete objects | Decision of incomplete objects |
|-------------------------------|----------------------|----------------|------------------------------|-------------------------------|
| P1                            | P2                   | 1              | soft contact lenses         | no contact lenses             |
|                               | P3                   | 1              | no contact lenses           |                              |
| P7                            | P8                   | 1              | hard contact lenses         | no contact lenses             |
|                               | P9                   | 1              | no contact lenses           |                              |
5. Conclusion

By converting the qualitative information system tables into binary tables, we can make a reduction of condition attributes and can predict the missing values of decision attribute according to the distance function and the most common values. This method provides us a new technique, which predicts the missing values according to the real data instead of making a mapping from the qualitative values to numbers.

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