Impacts of new small-scale N-body simulations on dark matter annihilations constrained from cosmological 21cm line observations

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We revisit constraints on annihilating dark matter based on the cosmological global 21cm signature observed by EDGES. For this purpose, we used the numerical data of the latest N-body simulation for the first time performed by state-of-the-art standard in order to estimate the boost factor at high redshifts (z = 10 – 100), which enhances the annihilation of dark matter in course of structure formations. By taking into account to what fraction injected energy from dark matter annihilation contributes to ionization, excitation, and heating of intergalactic medium during dark ages, we estimated how large the global 21cm absorption can be. In the thermal freezeout scenario, we find that the dark matter masses \( m_{\text{DM}} < 15 \text{ GeV} \) and \( m_{\text{DM}} < 3 \text{ GeV} \) have been excluded at 95% C.L. for the modes into \( \bar{b}b \) and \( e^+e^- \), respectively, which are obtained independently of any uncertainties in local astrophysics such as observationally-fitted density profiles of dark matter halos.

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I. INTRODUCTION

In scenarios of dark matter (DM) for the weakly-interacting massive particle (WIMP) [1], a DM particle with mass of the weak scale should have a thermally-averaged annihilation cross-section of the order of \( \langle \sigma v \rangle = 2 \times 10^{-26} \text{cm}^3/\text{sec} \) [2, 3]. This value is called the “canonical annihilation cross-section” and is obtained to agree with the observed abundance of DM which was produced from the thermal bath in the early Universe by the thermal freezeout mechanism (e.g., see Ref. [3] and references therein). Nowadays, a lot of new experimental projects have been proposed to observe signatures of annihilating DM, which heightens the momentum toward cosmologically verifying the existence of the WIMP DM.

On the other hand, it is still an open question how density fluctuations of DM can evolve nonlinearly at high redshifts \( z = O(10) – O(10^2) \) and form structures at small scales down to \( k \sim 10^6 – 10^7 \text{Mpc}^{-1} \) because nonlinear evolution of the density fluctuations becomes important. Actually two of the authors (KK and RT) of this paper have performed the detailed N-body simulation of cold DM (CDM) in a separate paper [4]. As a result, they are suggesting that the halo formation is really sizable even at such a high redshift epoch. The results of Ref. [4] enables us to calculate the boost factor as a function of redshift with a sufficient level of precisions. It is a striking point that this result means that DM could have inevitably annihilated at the high redshifts, and the energy injection by the annihilating DM is expected to be the order of \( O(10^{-21}) \text{eV/sec/cm}^3 \) at \( z \sim 20 \), which affects the absorption feature of the global 21cm line-spectrum (e.g., see Refs. [5–9] and references therein).

So far, the Experiment to Detect the Global Epoch of Reionization Signature (EDGES) collaboration reported the observational data for the absorption feature of the cosmological global 21cm line-spectrum [10] at around \( z \sim 17 \). In a pioneering work [6], by using this data the authors obtained upper bounds on the annihilation cross-section of DM in order not to reduce the trough of the absorption feature due to the extra heatings by the annihilations. The boost factors adopted in [6] were taken from the values from the following two papers with assuming somehow aggressive levels of model-dependent approximations: i) Ref [11] in which the Press-Schechter mass function formalism [12] with

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the Navarro-Frenk-White (NFW) halo profile [13] was assumed, and ii) Ref. [15] in which a halo model with the Einasto profile [14] was assumed. \(^1\)

On contrary to those previous works, we compute the boost factor as a function of \(z\) by adopting the raw numerical data of the detailed N-body simulations at the small scales reported in [4]. By using this boost factor, we update the upper bounds on annihilating DM with the modes into \(W^+W^-, bb, e^+e^−\) and \(γγ\) as conservatively as possible.

This paper is organized as follows. In Section II, we review how energy injection in general affects the evolution of the intergalactic medium (IGM). In Section III, we review how high energetic injection from DM annihilation is deposited into IGM. In Section IV, we describe how we estimate the annihilation boost factor based on our dedicated N-body simulation. In Section V, we present our results. We conclude in the final section.

II. EVOLUTION EQUATIONS OF IGM IN THE PRESENCE OF ENERGY INJECTION

In this section, we review how energy injection in general takes part in evolution of IGM. For illustrative purpose, we here follow the simple description of hydrogen in IGM based on the effective three-level atom model [28–30]. In numerical calculation we present in Section V, we adopt the recombination code \texttt{HyRec}\(^3\), which is based on the state-of-the-art effective multi-level atom model (See [31, 32] for details). We in this paper focus only on hydrogen ionization assuming helium is neutral, which should be a good approximation as long as we are interested in the Dark Ages [15] (See also [33]).

The evolution of ionization fraction, \(x_e\), is then described by the following equation:

\[
\frac{dx_e}{dt} = -C \left[ \alpha_H(T_m)x_e^2n_H - \beta_H(T_γ)(1-x_e)e^{-E_α/T_γ} \right]
\]

\[
+ \frac{dE_{\text{inj}}}{dVdt} \frac{1}{n_H} \left[ \frac{f_{\text{ion}}(t)}{E_0} + (1-C)f_{\text{exc}}(t) \right],
\]

where \(T_m\) and \(T_γ\) are respectively the temperatures of gas and photon, \(n_H\) is the number density of hydrogen, \(E_0 \simeq 13.6\, \text{eV}\) is the ionization energy of hydrogen, \(E_α = 3E_0/4\) is the energy of Ly-\(α\) photon, \(α_H\) is the case-B recombination coefficient and \(β_H\) is the corresponding ionization rate. The Peeble’s \(C\)-factor, which represents the probability that a hydrogen atom initially in the \(n = 2\) shell reaches the ground state without being photoionized, is given by

\[
C = \frac{Λn_H(1-x_e) + \frac{1}{2π2}E_α^3H(t)}{Λn_H(1-x_e) + \frac{1}{2π2}E_α^3H(t) + β_Hn_H(1-x_e)},
\]

where \(Λ \simeq 8.23\, \text{s}^{-1}\) is the two-photon decay rate of the hydrogen 2s-state, and \(H(t)\) is the Hubble expansion rate. The last term in (1) represents the effects of energy injection, which we will describe shortly after.

The evolution of the gas temperature \(T_m\) is described by the following equation:

\[
\frac{dT_m}{dt} = -2H(t)T_m + Γ_C(T_γ - T_m) + \frac{dE_{\text{inj}}}{dVdt} \frac{1}{n_H} \frac{2f_{\text{heat}}(z)}{3(1+x_e+f_{\text{He}})},
\]

where \(Γ_C\) is the coupling rate of \(T_m\) to \(T_γ\), which is predominated by the Compton scattering,

\[
Γ_C = \frac{8σ_T a_e T_γ^4}{3m_e} \frac{x_e}{1+f_{\text{He}}+x_e},
\]

where \(σ_T\) is the Thomson scattering cross section, \(a_e\) is the radiation constant, \(m_e\) is the electron mass, and \(f_{\text{He}}\) is the number ratio of helium to hydrogen.

\(^1\) About other related works to constrain DM from the data of EDGES, see also the following papers and references therein, Refs. [8]–[17] for annihilations, Refs. [8]–[9] [18]–[19] for decays, and Refs. [20]–[23] for DM-baryon interactions. And see also Refs. [24]–[26] for productions of additional photons to fit the EDGES data.

\(^2\) And also see Refs. [27] for constraints on the curvature perturbation at small scales from gamma-ray and neutrino observations produced in ultracompact minihalos of annihilating dark matter at present, which were calculated analytically by the Press-Schechter formalism while keeping the annihilation cross section to be the canonical one.

\(^3\) \url{https://pages.jh.edu/~yalihai1/hyrec/hyrec.html}
The last term in each of Eqs. (1) and (3), which is proportional to the energy injection rate per unit volume per time, \( \frac{dE_{\text{inj}}}{dVdt} \), represents the effect of energy injection. As defined in \[44, 60\] the coefficients \( f_{\text{ion}}(t), f_{\text{exc}}(t), \) and \( f_{\text{heat}}(t) \) (collectively denoted by \( \{f_c(t)\} \) hereafter) are the fractions of injected energy deposited into the hydrogen ionization, the hydrogen excitation and the heating of gas, respectively, which will be discussed in the next section.

### III. ENERGY INJECTION AND DEPOSITION INTO IGM FROM DM ANNIHILATION

In the case of DM annihilation, the energy injection rate is given as

\[
\frac{dE_{\text{inj}}}{dVdt} = \bar{\rho}_{\text{DM}} B(z) \langle \sigma v \rangle m_{\text{DM}},
\]

where \( \bar{\rho}_{\text{DM}} \) is the mean energy density of DM. \( B(z) = \langle \rho_{\text{DM}}^2 \rangle / \bar{\rho}_{\text{DM}}^2 \) is the boost factor due to the inhomogeneity of DM distribution, which will be discussed in Section IV. \( \langle \sigma v \rangle \) is the annihilation cross-section averaged over the phase space distribution and \( m_{\text{DM}} \) is the DM mass.

The deposition fractions \( \{f_c(t)\} \) depend on particle constituents and their energy spectra from DM annihilation as well as their interaction with IGM. We compute \( \{f_c(t)\} \) stepwise as follows:

1. Once the primary annihilation processes (e.g. DM + DM \( \rightarrow \) SM + SM) are specified, the standard model (SM) particle constituents and their energy spectra of the final state can be computed based on Monte Carlo event generators (e.g. PYTHIA\(^5\) and HERWIG\(^6\)) which can simulate cascades of primary annihilation products into stable SM particles. In this paper, for \( m_{\text{DM}} \) above 5 GeV we adopt PYTHIA to compute the energy spectra (For details, we refer to \[33–35\] and reference therein).

On the other hand, for \( m_{\text{DM}} \) below 5 GeV, where we in this paper restrict ourselves to primary annihilation channels into \( e^+e^- \) and \( \gamma\gamma \), we omit final state radiations and adopt monochromatic energy spectra from the primary annihilation processes. Since the fraction of energy carried by final state radiations is small and primary annihilation products efficiently deposit their energy into IGM at low energy, our treatment should be a good approximation.

2. Energetic electrons, positrons and photons ejected from DM annihilation subsequently interact with IGM. How those energetic particles lose their energy through interaction with IGM and affect ionization and heating of IGM have been studied by many authors, e.g., \[11, 36–42\]. Energetic electrons/positrons lose their energy on timescales shorter than the Hubble time. Meanwhile, the timescale of energetic photons above \( \approx 10^3 \) eV and below \( \approx 10^{11} \) eV can be longer than the Hubble time, which requires detailed computation of energy deposition over cosmological timescales. In this paper, we adopt the results of \[44\], which treats the effects of energy injection at linear level. For full treatments including feedback of modification of IGM evolution in computation of \( \{f_c(t)\} \) we refer to \[45\].

Analytically, we can estimate the energy injection rate to be

\[
\frac{dE_{\text{inj}}}{dVdt} \sim 10^{-21} \text{eV/sec/cm}^3
\]

\[
\times \left( \frac{B(z)}{10^2} \right) \left( \frac{1 + z}{18} \right)^6 \left( \frac{\langle \sigma v \rangle}{2 \times 10^{-26} \text{ cm}^3/\text{sec}} \right) \left( \frac{\Omega_{\text{DM}} h^2}{0.12} \right)^2 \left( \frac{m_{\text{DM}}}{10^2 \text{GeV}} \right)^{-1}.
\]

This order-of-magnitude energy injection rate can affect the absorption feature of the global 21cm line spectrum \[5–9\].

### IV. N-BODY SIMULATION AND THE ANNIHILATION BOOST FACTOR

DM annihilation is enhanced by inhomogeneity in DM distribution, which can be encapsulated in the boost factor \( B(z) \). Even at redshifts as high as \( z \gtrsim 15 \) which we are focusing on in this paper, DM fluctuations at small scales have

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\(^4\) Here DM is assumed to be self-conjugate.

\(^5\) http://home.thep.lu.se/~torbjorn/Pythia.html

\(^6\) https://herwig.hepforge.org

\(^7\) https://faun.rc.fas.harvard.edu/epsilon/
grown to be nonlinear. Therefore, to estimate \( B(z) \), one needs to trace the nonlinear evolution of DM fluctuations. N-body simulations have been a powerful tool for this purpose.

Denoting \( \delta(x; z) \) as the DM density contrast at a spatial position \( x \) at redshift \( z \), the boost factor is defined as \( B(z) = 1 + \langle \delta^2(x; z) \rangle \). It can be recast using the Fourier transform as \[ B(z) = 1 + \int_0^\infty \frac{dk}{k} \Delta^2(k; z), \] (7)

with \( \Delta^2(k; z) \equiv k^3 P(k; z)/(2\pi^2) \) where \( P(k; z) \) is the power spectrum of DM density fluctuations. The dimensionless power spectrum \( \Delta^2(k; z) \) is almost flat at \( k \gtrsim 10 \text{ Mpc}^{-1} \), where horizon crossing takes place during the radiation dominated era. Therefore, the expression indicates that \( B(z) \) is contributed from a wide range of scales. This necessitates that N-body simulations should be performed with a variety of box-sizes, enabling DM fluctuations to be resolved at relevant scales. However, so far there have been few studies performing N-body simulations as such focusing on redshifts of our interest. In [4], some of the authors of this paper have addressed this issue by performing dedicated N-body simulations.

As presented in [4], a suite of cosmological N-body simulations with a variety of box-sizes (i.e., side lengths of cubic boxes) is performed. The box-sizes range from 1 kpc to 10 Mpc to cover a wide range of scales, \( k \approx 1-10^7 \text{ Mpc}^{-1} \). The simulations are comprised of 2560^3 collisionless particles. The initial linear power spectrum is prepared using the transfer function [53] with the free streaming damping of DM particles at \( k_{fs} = 10^6 \text{ Mpc}^{-1} \) [54]. Initial conditions of the simulations are set at redshift \( z = 400 \) based on the second-order Lagrangian perturbation theory [55, 56]. We employed the gravity solver GreeM [57] to follow the nonlinear gravitational evolution. To compute the boost factor, \( \Delta^2(k) \) is constructed by connecting estimated DM power spectra at different wave number bands that depend on box-sizes of simulations. For more details of the simulations and analyses, we refer to [4].

Figure 1 shows \( B(z) \) computed by using data of the simulations. As references, the figure also shows \( B(z) \) computed based on linear perturbation theory as well as one based on the halo model in [50], which is referred to as the "Boost 1" model in [6].

Here, in the linear theory, \( B(z) - 1 \) simply evolves as \((1 + z)^{-2}\). Compared to other estimations, e.g. the "Boost 1" model adopted in [6] as a conservative choice, our \( B(z) \) is smaller than it at \( z \lesssim 50 \). This results in suppressed DM annihilation rate and hence may lead to much more conservative upper bounds on dark matter annihilation cross-section.

V. RESULTS

In figure 2 we demonstrate the evolution of \( x_e(z) \) and \( T_m(z) \) in the presence of DM annihilation with DM mass \( m_{DM} = 100 \text{ GeV} \). We here assume that there is no significant heating from astrophysical sources.

The differences between the results of the linear theory and the N-body simulation for the \( W^+W^- \) and \( b\bar{b} \) emissions are larger than the ones for the line \( e^+e^- \) and \( \gamma\gamma \) emissions. That is because more soft daughter electromagnetic particles such as \( e^+e^- \) or \( \gamma\gamma \) are produced through cascade decays of unstable mesons and baryons in cases for the
$W^+W^-$ and $b\bar{b}$ emissions, compared with the cases for the line $e^+e^-$ and $\gamma\gamma$ emissions. Then, the energy-deposition is more efficient for $W^+W^-$ and $b\bar{b}$ due to the delayed deposition \cite{16}.

$T_m$ is increased compared to cases where energy injection from dark matter annihilation is absent, which should result in modified evolution of the spin temperature, $T_s$, associated with the hyperfine splitting of neutral hydrogen ground states. This allows us to constrain DM annihilation cross-section from observations of differential brightness temperature of redshifted 21 cm line emission

$$T_{21\text{cm}}(z) = \frac{T_s(z) - T_\gamma(z)}{1 + z} T_{21\text{cm}}(z), \quad (8)$$

before reionization (See e.g. \cite{37}). The time-evolution of $T_s$ in general depends on relative couplings of $T_s$ with $T_\gamma$, $T_m$ and the color temperature $T_c$, which is the effective temperature associated with background Lyman-\(\alpha\) radiation. As IGM is always optically thick for Lyman-\(\alpha\) radiation during the cosmological epoch we are interested in, it is reasonable to assume $T_c \approx T_m$. The fact that EDGES has reported a global absorption signal \cite{10}

$$T_{21\text{cm}} = -500^{+300}_{-200} \text{mK} \quad (99\% \text{ CL}), \quad (9)$$
indicating $T_m < T_\gamma$, then the upper bounds on the DM annihilation cross-section should exist. This is because DM annihilation in general suppresses the absorption amplitude of global 21cm signals by ionizing and heating IGM. In Figure 2 the differences between the solid and dotted lines look much smaller than the ones directly-expected from the face values of the difference between the two lines in the boost factors from our N-body simulations and linear perturbation calculations in Figure 1. That is because the delayed deposition occurred as was discussed in Ref. [46, 58].

We in particular obtain conservative upper bounds on DM annihilation cross-section by maximizing the absorption amplitude in the absence of DM annihilation. This can be realized by assuming no heating of IGM other than DM annihilation. We also assume tight coupling of spin temperature to gas temperature via Lyman-\(\alpha\) pumping (Wouthuysen-Field effect [48, 49]), which can also maximize the absorption depth. Figure 3 shows upper bounds on DM annihilation cross-section based on this strategy. Our baseline calculation in the absence of DM annihilation, gives $T_{21\text{cm}} \simeq -230\text{ mK}$. We put upper bounds on the annihilation cross-section of the DM by requiring $T_{21\text{cm}} \leq -75\text{ mK}$, which correspond to the 2\sigma bound given uncertainties of EDGES.

From this figure, we find that the upper bounds on the annihilation cross sections, which are conservatively-obtained in this study for the $b\bar{b}$, $e^+e^-$ and $\gamma\gamma$ modes, are milder than the ones in the results of [6]. That is because the boost factor we adopted is smaller than the ones in [6]. When we assume the canonical value of the annihilation cross-section, $\langle \sigma v \rangle = 2 \times 10^{-26}\text{ cm}^3/\text{sec}$, we can exclude the masses of DM for each mode to be $m_{\text{DM}} < 15\text{ GeV}$ ($b\bar{b}$), $m_{\text{DM}} < 3\text{ GeV}$ ($e^+e^-$), and $m_{\text{DM}} < 1\text{ GeV}$ ($\gamma\gamma$) at 95% C.L.

VI. CONCLUSION

In this paper we have revisited the possible constraints on annihilation cross-sections of DM from the observations on the cosmological global 21cm line-spectrum reported by EDGES. By adopting the latest data of high-redshift dark-matter halo-formations ($z = O(10) - O(10^2)$) performed by the detailed N-body simulations at the small scales, we have updated the boost factor of the annihilating DM due to the clumpiness.

With this updated value of the boost factor, we obtained the more conservative upper bounds on the annihilation cross-sections than the previous work. In this study, we can exclude the masses of DM for $m_{\text{DM}} < 15\text{ GeV}$ ($m_{\text{DM}} < 3\text{ GeV}$) at 95% C.L. for the mode into $b\bar{b}$ ($e^+e^-$) by assuming the canonical value of the annihilation cross-section, $\langle \sigma v \rangle = 2 \times 10^{-26}\text{ cm}^3/\text{sec}$. These bounds obtained from the global 21cm spectrum are cosmologically robust along with the ones from CMB [60] and BBN [59] because they do not depend on local astrophysical uncertainties.

In the future, we can improve sensitivities on the constraints on the annihilation cross-section by adopting more precise observational data which are expected to be reported by new projects such as HERA [61], SKA [62], Omnis-
cope or DAPPER.

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