EMOGI: Efficient Memory-access for Out-of-memory Graph-traversal In GPUs

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ABSTRACT
Modern analytics and recommendation systems are increasingly based on graph data that capture the relations between entities being analyzed. Practical graphs come in huge sizes, offering massive parallelism, and are stored in sparse-matrix formats such as compressed sparse row (CSR). To exploit the massive parallelism, developers are increasingly interested in using GPUs for graph traversal. However, due to their sizes, graphs often do not fit into the GPU memory. Prior works have either used input data pre-processing/partitioning or unified virtual memory (UVM) to migrate chunks of data from the host memory to the GPU memory. However, the large, multi-dimensional, and sparse nature of graph data creates a major challenge to these schemes and results in significant amplification of data movement and reduced effective data throughput. In this work, we propose EMOGI, an alternative approach to traverse graphs that do not fit in GPU memory using direct cache-line-sized access to data stored in host memory.

This paper addresses the open question of whether a sufficiently large number of overlapping cache-line-sized accesses can be sustained to 1) tolerate the long latency to host memory, 2) fully utilize the available bandwidth, and 3) achieve favorable execution performance. We analyze the data access patterns of several graph traversal applications in GPU over PCIe in an FPGA to understand the cause of poor external bandwidth utilization. By carefully coalescing and aligning external memory requests, we show that we can minimize the number of PCIe transactions and nearly fully utilize the PCIe bandwidth with direct cache-line accesses to the host memory. EMOGI achieves 2.92x speedup on average compared to the optimized UVM implementations in various graph traversal applications. We also show that EMOGI scales better than a UVM-based solution when the system uses higher bandwidth interconnects such as PCIe 4.0.

1 INTRODUCTION
Graph workloads are becoming increasingly widespread and common in various applications such as social network analysis, recommendation systems, financial modeling, bio-medical applications, graph database systems, web data, geographical maps, and many more [10–14, 16, 43, 46, 52]. Graphs used in these applications often come in huge sizes. A recent survey conducted by the University of Waterloo [46] finds that many organizations use graphs that consist of billions of edges and consume hundreds of gigabytes of storage.

The main challenge that graph application developers currently face is performing graph traversal computations on large graphs [46]. Because of the massive parallelism present in the graph traversal computation, GPUs are increasingly used to perform graph analytics. However, the ability to process large graphs in GPUs is currently hampered by their limited memory capacity. Thus in this work, we primarily focus on developing an efficient graph traversal system using GPUs that access large graph data from host memory.

For efficient storage and access, graphs are stored in a compressed sparse row (CSR) data format as it has low memory overhead. In CSR format, a graph is stored as the combination of a vertex list and an edge list. Even with CSR data format, large graph datasets cannot fit in today’s GPU memory. Thus, most prior works store these large graphs in host memory and have GPUs access them through the unified virtual memory (UVM) mechanism [8, 9, 21, 26, 29, 32, 33, 35]. UVM brings both CPU memory and GPU memory into a single shared address space. UVM allows GPUs to simply access the data in the unified virtual address space and it transparently migrates required pages between host memory and GPU memory using a paging mechanism.

However, several prior work [8, 9, 21, 29, 32, 33, 35] have reported that the performance of graph traversal using UVM is not competitive. This is because memory accesses that go to the edge list during graph traversal are irregular in nature. Furthermore, based on our analysis of 1122 graphs that have at least 1M vertices and edges from LAW [11], SuiteSparse Matrix Collection [16], and Network Repository [43], we find the average degree per vertex is about 71. This implies that when those graphs are represented in a compressed adjacency list format such as CSR, each vertex’s neighbor edge list is about 71 elements long on average. Thus transferring an entire 4KB page, as in the case of UVM, can cause memory thrashing and unnecessary I/O read amplification.

As a result, prior works have proposed pre-processing of input graphs by partitioning and loading those edges that are needed during the computation [24, 45, 47, 50] or proposing UVM specific hardware or software changes such as locality enhancing graph
reordering [21], GPU memory throttling [32, 33], overlapping compute and I/O [23], or even proposing new prefetching policies in hardware that can increase data locality in GPU memory [8, 9, 29].

In this work, we take a step back and revisit the existing hardware memory management mechanism for when data does not fit in GPU memory. Specifically, we focus on zero-copy memory access which allows GPUs to directly access the host memory in cache-line granularity. With zero-copy memory access, no complicated data migration is needed and GPUs can fetch data as small as 32-byte from the host memory. Even with such advantages, unfortunately, zero-copy is known to have overwhelmingly performance due to the low external interconnect bandwidth [20]. Interestingly, however, we do not find any systematic analysis showing the exact limiting factor of the zero-copy performance or leading to any effort to improve it.

Instead of making a premature conclusion, we build a system with a custom-designed FPGA-based PCIe traffic monitor and explore any opportunity to optimize zero-copy performance. We use the system to address the question of whether a sufficiently large number of overlapping cache-line-sized accesses can be sustained to 1) tolerate the long latency to host memory, 2) fully utilize the available bandwidth, and 3) achieve favorable execution performance for graph traversal applications. To this end, the key goal of our work is to avoid performing any pre-processing or data manipulation on the input graph and allowing GPU threads to directly perform cache-line-sized accesses to data stored in host memory during graph traversals.

By using a toy example, we show that by naively enabling zero-copy, the system cannot saturate the PCIe 3.0 x16 bandwidth (see § 3.3). To address this, we propose two key software optimizations needed to best exploit PCIe bandwidth for the zero-copy access. First, we propose the merged memory access optimization that optimizes for generating maximum-sized PCIe request to zero-copy memory (see § 3.3). Second, we propose forcing memory access alignment by shifting all warps to 128-byte boundaries when there is misalignment. This is because the memory access merge optimization does not guarantee memory request alignment. Such misalignment can result in performance degradation. While these optimizations sacrifice some parallelism and incur additional control divergence during kernel execution, their benefit in terms of improved bandwidth utilization far outweighs the cost. We then apply these two optimizations to popular graph traversal applications including breadth-first search (BFS), single-source shortest path (SSSP), and connected components (CC) to enable efficient traversal on large graphs.

Using real-world and synthetic large graphs (see Table 2), we show that EMogi can achieve 2.93× speedup on average compared to the optimized UVM implementations of BFS, SSSP and CC benchmarks across a variety of graphs. We also evaluate EMogi on the latest generation of the NVIDIA Ampere A100 GPU with PCIe 4.0 and show that EMogi still remains performant and scales better than the UVM solution when using higher-bandwidth interconnect. EMogi achieves speedups of up to 4.73× over current state-of-art GPU solutions [21, 45] for large out-of-memory graph traversals. In addition, EMogi does not require preprocessing or runtime page migration engine.

To the best of our knowledge, EMogi is the first work to systematically characterize GPU PCIe access patterns to optimize zero-copy access and to provide in-depth profiling results of varying PCIe access behaviors for a wide range of graph traversal applications. Overall, our main contributions can be summarized as follows:

1. We propose EMogi, a novel zero-copy based system for very large graph traversal on GPUs.
2. We propose two zero-copy optimizations, memory access merge and memory access alignment, that can be applied to graph traversal kernel code to maximize PCIe bandwidth.
3. We show EMogi performance scales linearly with CPU-GPU interconnect bandwidth improvement by evaluating PCIe 3.0 and PCIe 4.0 interconnects.

The rest of the paper is organized as follows: we provide a brief primer on GPU based graph traversal and the challenges in executing graph traversals using UVM in § 2. We then discuss how to enable zero-copy memory with GPUs and discuss the reasons for its poor performance in a naive but common kernel code pattern in § 3. Using the gained insights, we then apply zero-copy optimizations to graph traversal algorithms in § 4. We discuss EMogi’s performance improvement for various graph traversal algorithms on several large graphs in § 5. § 7 discusses how EMogi differs from prior work and we conclude in § 8.

2 BACKGROUND

In this section, we first provide a brief primer on GPU based graph traversal. Then we will describe techniques used to traverse graphs that cannot fit into the GPU memory.

2.1 Parallelizing Graph Traversal on GPUs

Graph traversals can be largely divided into a vertex-centric [25, 31, 49] method and an edge-centric [44] method. The vertex-centric method can be further divided into a scatter-based method and a gather-based method. In this paper, we mainly focus on the vertex-centric + scatter method due to its simplicity.

The exact workflow of the graph traversal highly depends on the type of the application and the optimization level, but a general flow can be described with Algorithm 1. First, before the traversal begins, initial active vertices need to be set. In the case of BFS, only a single vertex needs to be set as active, which is basically a source

```
Algorithm 1: High-level Graph Traversal Flow

set_initial_active_vertex()

for all vertices v1 in Graph G do
    if v1 is active then
        set v1 as inactive
        for all neighbors v2 of v1 do
            application_dependant_workload()
            if application_dependant_condition() then
                set v2 as active
            end
        end
    end
end
```
The condition to set the next active vertices depends on the type of application as well. In the case of BFS, any neighboring vertices which are not visited ever before are marked to be the next active vertices. The traversal ends once there are no more active vertices left in the graph.

The main benefit of the GPU implementation of the graph traversal comes from the massive number of vertices [13, 14, 52]. With a help of several atomic instructions (may not be necessary), both the inner loop and the outer loop in Algorithm 1 can be fully parallelized with GPU for various kinds of graph traversal applications [15, 25, 27, 28].

As an input graph format for the GPU graph traversal, we use compressed sparse row (CSR) format. CSR is arguably the most popular way to represent a graph because of its low memory overhead [24, 41, 45, 47, 50, 55]. CSR encodes the entire graph with just 2 arrays, as shown in Figure 1. The edge list stores each vertex’s neighbor list contiguously, such that all the neighbors of vertex 0 are stored first, then the neighbors of vertex 1, and so on. The vertex list is indexed by a vertex ID and stores the starting offset of that vertex’s neighbor list in the edge list. When there are any additional vertex and edge values such as weights, they can be either combined with the existing lists by forming tuples or a separate dedicated list can be allocated.

2.2 Out-of-Memory Graph Traversal on GPUs

Graphs, even in the CSR format, can be orders of magnitude larger than GPU memory. The easiest way to enable GPU based graph traversal on such graphs is to use the Unified Virtual Memory (UVM) [1, 2, 8, 9, 21, 26, 29, 32, 33, 35, 42]. UVM is a unified memory management module that provides a single memory address space accessible by both CPU and GPU through the page faulting mechanism. UVM reduces the burden on the programmer as they do not have to explicitly manage where the data resides. UVM transparently allows device memory over-subscription with the use of CPU memory, enabling computation on large data sets that exceed GPU device memory capacity. The UVM driver is responsible for on-demand page migration between the CPU and GPU.

The inefficiency of UVM in graph traversal comes in two ways. First, for the very large graphs, it is hard to exploit temporal locality as the limited GPU memory capacity will cause frequent page thrashing. Second, there is a lack of spatial locality between the neighbor lists of vertices being visited in an iteration, causing significant I/O read amplification and more frequent page migrations. For example, in Figure 1, the neighbor lists of the vertex 1 and 3 need to be accessed at the same time we start BFS from the vertex 4. However, as shown in the CSR representation, the lists are non-contiguous in the edge list. In a more realistic case with a large graph, these lists can be separated by millions of elements in the edge list. Therefore, accessing these two lists will likely generate two separate 4KB page migrations. Assuming that all accesses to the different neighbor lists will generate separate 4KB page migrations, all neighbor lists should have least 512 to 1024 of elements (depends on the datatype size) to make the 4KB data transfer 100% efficient, which might be quite challenging. By combining the frequent page migrations caused by the lack of data locality and the high page fault handling overhead of UVM, GPU performance can be severely throttled.

3 ZERO-COPY

To allow GPU threads access to the external memory in smaller granularity than UVM, GPUs support marking memory address ranges as zero-copy memory [3]. Zero-copy, also often referred to as direct access, does not require any page migration or duplication between the external and GPU memories. Instead, GPU threads access zero-copy memory as if it was GPU global memory, and the GPU transforms memory requests from the threads to memory requests over an external interconnect like PCIe. The target of the memory requests can be anywhere in the system as long as the location can be memory-mapped into the shared bus address. Common examples include system memory, peer-connected PCIe network interface card, and peer-connected GPU. Due to the high latency of the external interconnects, using zero-copy was thought to have low bandwidth [20] and thus often used for only accessing...
small or infrequently accessed data. In this section, we describe how to
enable zero-copy and use a peer-connected FPGA to explore any
optimization opportunities available for zero-copy in detail. Based
on the analysis, we show several essential optimization techniques
to maximize the zero-copy bandwidth. With proper implementation,
zero-copy can nearly saturate the PCIe bandwidth.

3.1 Enabling Zero-Copy

From the system’s point of view, zero-copy is enabled as follows:
First, the data to be shared with GPU must be pinned in the host
memory. Pinned memory cannot be swapped out to the disk or
relocated by the host OS memory manager. Second, the correspond-
ing bus address (e.g., PCIe) of the pinned data should be mapped
into the GPU page table so the GPU can generate a correct external
memory request. Finally, the mapped address should be passed
into the userspace so the programmer can use pointers in the GPU
kernel to access the region.

From CUDA API’s point of view, zero-copy can be enabled in
three ways. First technique uses cudaMallocManaged() to allocate
UVM space and applies cudaMemAdviseSetAccessedBy flag with
cudaMemAdvise(). The resulting data pointer can be directly used
from CUDA kernels to generate zero-copy memory access. One
thing worth noting here is that the cudaMemAdviseSetAccessedBy
flag should not be used with other cudaMemAdvise() flags since
the other flags override cudaMemAdviseSetAccessedBy. Second is
by using cudaMallocHost(). This is the simplest method since the
memory allocated by cudaMallocHost() can be directly used in
the CUDA kernel to do zero-copy access. The last scheme uses gen-
eral memory allocators, like malloc(), and cudaHostRegister() and
cudaGetDevicePointer() on top of the allocated memory.
In this case, the cudaHostRegister() pins the allocated memory
space and cudaGetDevicePointer() returns a CUDA-compatible
pointer. Our experiments showed all three techniques provided the
same performance.

3.2 Zero-Copy Analysis Setup

To understand how GPU accesses external zero-copy memory over
PCIe, we designed and built the monitoring system shown in
Figure 2. The FPGA is connected to the GPU using a PCIe switch
in peer-to-peer mode. Furthermore, the FPGA is programmed to
advertise itself as a large memory using the base address register
(BAR) region provided by the PCIe specification [7]. This advertised
FPGA memory region can be mapped to the user space using the
mmap() system call. The returned pointer value from the mmap()
Merged and Aligned Access: In this case, threads are grouped into warps, with each warp containing 32 threads, and the threads in a warp access consecutive elements in a 128-byte cacheline of the input array. This allows the GPU coalescing unit to automatically merge the contiguous 32-byte memory requests into a single larger 128-byte PCIe request (Figure 3 (b)). With 128-byte PCIe requests, it becomes much easier to reach the maximum PCIe bandwidth. First, the PCIe TLP overhead ratio decreases from 36% to 12.3%. Second, having only 135 PCIe outstanding requests is sufficient to reach 16GB/s of bandwidth (without considering other PCIe overheads). Lastly, 128-byte is a multiple DRAM request size and therefore there is no inefficiency in the DRAM interface. In Figure 4 (b), we see this approach can saturate the PCIe bandwidth at about 12.23GB/s, matching the measured bandwidth when using the cudaMemcpy() API to perform a block data transfer.

Merged but Misaligned Access: However, for all practical purposes, guaranteeing 128-byte alignment for any data structure can be difficult. It is possible that the starting index of a warp is not aligned with the 128-byte boundary. Some warps may need to make two separate PCIe requests to fetch a single 128-byte cacheline. In the worst case, if a warp’s memory access is not 128-byte aligned and warps access contiguous regions of memory, the misalignment can be cascaded to all subsequent warps. Unfortunately, this results in all warps generating two PCIe requests. In Figure 3 (c), we show an emulated misaligned case where each warp is intentionally accessing memory offset by 32-byte from 128-byte boundary and therefore all warps end up generating a 32-byte and a 96-byte PCIe request. From Figure 4 (c), we can see the achieved PCIe bandwidth is lower than the aligned case. To avoid this, either the starting index of warps should be shifted or the input data must be shifted in memory so the data accessed first is 128-byte aligned.

4 EMOGI: ZERO-COPY GRAPH TRAVERSAL

Now that we understand zero-copy memory and its characteristics, we discuss how to efficiently use zero-copy memory for graph traversal when the graph cannot fit in the GPU memory. First, we describe the micro data locality we observed in graph traversal applications to justify why zero-copy should perform better than UVM (see § 4.1). Then, we introduce our baseline graph traversal algorithm (see § 4.2) and optimize it for zero-copy memory based on the knowledge we gathered from § 3.3 (see § 4.3).

4.1 Data locality in Graph Traversal

To exploit zero-copy for graph traversal, we preferably need at least 128-byte of spatial locality to best use each memory access. A single 128-byte zero-copy access can have 16 or 32 elements of data if the CSR data type is 8-byte or 4-byte, respectively. Compared to UVM, which requires at least 4KB of spatial locality (512 or 1024 elements of data), finding 16 to 32 elements of spatial locality is reasonable for the graphs we studied.

Based on our analysis of 1122 graphs from Network Repository [43], SuiteSparse Matrix Collection [16], and LAW [11], we
find the average degree per vertex is 71. This means, when those
graphs are represented in an adjacency list format like CSR, each
vertex’s neighbor list is 71 elements long on average. Considering
that graph traversal algorithms require scanning the entire neigh-
bor list of a vertex, we can obtain a spatial locality of 71 elements
on average in graphs. Such a spatial locality can benefit from effi-
cient 128-byte requests to zero-copy memory. In contrast, it is more
difficult to achieve the same level of efficiency using UVM since
the available spatial locality is significantly less than the required
512 or 1024 elements.

4.2 EMOGI Baseline
EMOGI assumes the input graph is stored in the memory using the
CSR data layout (see § 2.1). All input data structures are statically
mapped during initialization. The edge list is allocated in the host
memory as it doesn’t fit in GPU memory, but other small data
structures such as buffers and the vertex list are allocated in GPU
memory. It is worth noting that even for the biggest graphs we
evaluated (see § 5.2), the vertex list consumes at most about 1GB of
memory. Thus, GPU memory is sufficient for the vertex list.

EMOGI adopts vertex-centric graph traversal algorithms. For
every vertex that needs to be processed, a worker is assigned and
the worker traverses a neighbor list associated with the vertex in
the edge list. Listing 1 shows the pseudo-code of our naive baseline
implementation. Here, the worker is a single GPU thread and each
worker is assigned to the neighbor list associated with its corre-
sponding vertex. When each neighbor list is larger than 128-byte,
this baseline implementation has a similar memory access pattern
to the strided case explained in § 3.3.

Compared with the UVM approach, EMOGI’s graph traversal
approach removes the page faults from occurring and reduces the
I/O amplification as only the needed bytes are moved. In the vertex-
centric graph traversal approach, the input graph is traversed by a
single vertex depth on every kernel execution. Therefore the total
number of kernels launched, say in the case of breadth-first-search
(BFS), is equal to the distance between the source vertex to the
furthest reachable vertex.

4.3 Optimizations
Since the EMOGI baseline implementation is similar to the strided
case presented in § 3.3, it suffers from uncoalesced memory requests.
As we noted, without addressing this, one cannot generate efficient
PCIe requests to the zero-copy memory. In this subsection, we will
discuss how EMOGI addresses this limitation using the insights
from § 3.3 and modifying only the GPU kernel code of the traversal
application. Thus, it is entirely possible to package the proposed
optimizations into a library to lessen the programmer’s effort when
trying to exploit them.

4.3.1 Merged Memory Access: EMOGI performs merged memory
accesses in per vertex granularity, similar to [28]. The difference be-
tween EMOGI and [28] is that EMOGI always fixes the worker size
to an entire warp (i.e., 32 threads). Thus a whole warp is responsible
for traversing the neighbor list of one vertex. The specific imple-
mentation of this optimization is explained with red comments in
Listing 2. This allows EMOGI to always optimize for generating the
maximum sized PCIe request to the zero-copy memory. If the input

4.3.2 Aligned Memory Access. As we discussed in § 3.3, a misaligned access to the 1D data array can result in multiple smaller zero-copy requests. To address this, we have to not only merge memory accesses but align them as well. However, doing this on a CSR edge list is not straightforward. This is because CSR doesn’t align the edge list as alignment requires padding and thus increases memory footprint. Starting addresses of neighbor lists for graphs stored in CSR can be at any location in the memory.

One way to address this challenge is to pre-process the CSR graphs and align neighbor lists to 128-byte boundaries. However, this might incur excessive memory overhead. More importantly, one of the goals of this work is to avoid any pre-processing.

Therefore, instead of manipulating the input data, we force all warps to start from the closest preceding 128-byte boundary when there is misalignment. For instance, as shown in Listing 2 with blue comments, all starting indices fetched from the offset array is shifted to the closest 128-byte boundary before the list. With this change to the GPU kernel code, all subsequent warp memory accesses are guaranteed to have 128-byte alignment. Of course, some of the threads in the warp must be turned off during the first iteration of data fetching with a conditional statement to prevent reading unnecessary bytes. Similar to the memory access merge optimization, this additional conditional statement increases the occurrence of control divergence in CUDA kernels. However, due to the high external interconnect latency, it is more important to not miss any opportunity for generating large memory requests.

5 EVALUATION

Our evaluation shows that (1) EMOGI improves the performance of graph traversal algorithms by efficiently accessing the zero-copy memory for very large graphs, (2) EMOGI is mainly limited by the PCIe bandwidth and it scales almost perfectly linearly when PCIe 3.0 is replaced with PCIe 4.0, (3) EMOGI remains performant even with the latest generation of GPU NVIDIA Ampere A100 [5] and achieves better scaling compared to the UVM optimized implementation.

5.1 System Overview

5.1.1 System Overview: We use a Cascade-lake server machine with two 20 core Intel Xeon Gold 6230 CPUs equipped with 256GB of DDR4 2933MHz memory and an NVIDIA Tesla SXM2 V100 16GB GPU as our evaluation platform. The system is configured as shown in Figure 2. We use the FPGA only to analyze the zero-copy nature of DDR4 2933MHz memory and an NVIDIA Tesla SXM2 V100 16GB, 5120 CUDA cores

5.1.2 Systems Compared: To show the performance benefit of EMOGI, we use three different graph traversal algorithms: Breath-First Search (BFS), Single-Source Shortest Path (SSSP), and Connected Components (CC). We base our initial implementation of BFS and SSSP from [28, 37] while the CC baseline implementation is from [51]. We compare EMOGI with the following systems:

(a) UVM implementation stores the CSR edge list in the UVM address space while the vertex list is kept in the GPU memory. In addition, the CSR edge list in the UVM address space is marked as cudaMemAdviseSetReadMostly using the cudaMemAdvise() CUDA API call. This optimization allows the GPU to create a read-only copy of the accessed pages in the GPU’s memory. We also tested other available flags and UVM hints and we found that this configuration provided the best overall performance when using UVM.

(b) Naive implementation is the baseline implementation of EMOGI using zero-copy memory and is identical to Algorithm 1. In this implementation, the vertex list is stored in the GPU memory while the edge list is kept in the zero-copy host memory.

(c) Merged implementation of EMOGI merges the memory requests to the zero-copy memory, as discussed in § 4.3.1. However, in this implementation, there is no guarantee that accesses to the zero-copy memory are aligned.

(d) Merged+Aligned implementation is the fully optimized version of EMOGI where the memory accesses are not only merged but we force all warps to shift to the 128-byte boundary when there is a misalignment. This implementation is discussed in § 4.3.2.

5.2 Evaluation Datasets

For the evaluation, we use the graphs listed in Table 2. GK, GU, FS, and ML are the largest four graphs from SuiteSparse Matrix Collection [16] and SK, and UK5 are commonly used large graphs from LAW [11]. This collection of graphs covers data from different areas such as biomedicine, social networks, web crawls, and even synthetic graphs. All vertex and edge lists use 8-byte per element unless specified otherwise. All the graphs, except for SK and UK5, are undirected. We use the default weights for GU, GK, and ML graphs while we randomly initialize weights for the rest of the graph from the integer values between 8 to 72. Weights are represented in 4-byte datatype. The average degree of the graphs is 38, except for the ML graph, which has an average degree of 222. For fair BFS and SSSP performance evaluations, we pick 64 random vertices from each graph as the starting sources and reuse the selected vertices

Table 1: Evaluation system configuration.

| Category      | Specification                                      |
|---------------|----------------------------------------------------|
| CPU           | Dual Socket Intel Xeon Gold 6230 20C/40T           |
| Memory        | DDR4 2933MHz 256GB in Quad Channel Mode            |
| GPU           | Tesla V100 HBM2 16GB, 5120 CUDA cores              |
| OS            | CentOS 8.1.1911 & Linux kernel 5.5.13              |
| S/W           | NVIDIA Driver 440.82 & CUDA 10.2.89                |

Table 2: Graph Datasets. $V$ = Vertex, $E$ = Edge, and $w$ = Weight.

| Sym. | Graph                   | Number | Size (GB) |
|------|-------------------------|--------|-----------|
|      |                         | $V$ | $E$ | $|E|$ | $w$ | |
| GK   | GAP-kron [10]           | 134.2M| 4.22B| 31.5 | 15.7 |
| GU   | GAP-urand [10]          | 134.2M| 4.29B| 32.0 | 16.0 |
| FS   | Friendster [52]         | 65.6M | 3.61B | 26.9 | 13.5 |
| ML   | MOLIERE_2016 [48]      | 30.2M | 6.67B | 49.7 | 24.8 |
| SK   | sk-2005 [12–14]       | 50.6M | 1.95B | 14.5 | 7.3  |
| UK5  | uk-2007-05 [13, 14]   | 105.9M| 3.74B | 27.8 | 13.9 |

Category Specification

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OS CentOS 8.1.1911 & Linux kernel 5.5.13
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In this evaluation, we take BFS as an example and thoroughly evaluate PCIe traffic for request size distribution, achieved bandwidth, and the total amount of data transferred. Throughout the evaluation, we use the UVM implementation as the baseline.

5.3 Case-Study: Breadth-First Search

In this section, we take BFS as an example and thoroughly evaluate PCIe traffic for request size distribution, achieved bandwidth, and the total amount of data transferred. Throughout the evaluation, we use the UVM implementation as the baseline.

5.3.1 Zero-copy Request Size Distribution: In this evaluation, we show the impact of optimizing the memory access pattern from §3.3 on generating different sizes of PCIe request. The histogram of the PCIe request size is gathered using the FPGA monitoring platform explained in §3.2. In Figure 5, we show the breakdown of request sizes for all the PCIe requests from the three implementations: Naïve, Merged, and Merged+Aligned.

We observe in Figure 5 that nearly all PCIe requests in the case of Naïve implementation are of 32-byte granularity. This is because it is only possible to generate a PCIe request larger than 32-byte in the Naïve implementation when multiple neighbor lists happen to be spatially near in the edge list and they are accessed by multiple threads in a single warp. However, such a scenario is extremely unlikely. For example, we observe that only 1.3% of the PCIe requests from BFS on the FS graph are of a size bigger than 32-bytes.

When we analyze the request size distribution for the Merged and Merged+Aligned optimized implementations, we observe the following. First, although with the Merged approach the percent of 128-byte requests increases to about 40% on average, the percent of 128-byte requests is slightly higher than average for the ML graph, at about 46.7%. Second, when using the +Aligned approach on graphs that have most of their edges associated with high-degree vertices, we expect that most zero-copy memory requests should be for 128-bytes. This is expected because in the +Aligned implementation, zero-copy memory requests are merged and aligned to 128-byte granularity whenever possible. We observe this behavior for most graphs in Figure 5. For example, the percent of 128-byte requests improves by 1.86x for the GK graph between the Merged and +Aligned implementations. However, the percent of 128-byte requests improves by only 1.25x between the two implementations on the GU graph, a graph that has a similar number of edges and vertices as the GK graph.

To further analyze these behaviors, we plot in Figure 6, the cumulative distribution function (CDF) on the number of edges in each graph. CDF on the number of edges provides us a better understanding of the distribution of the neighbor list sizes in the graph. The horizontal axis of this CDF is cut to 96 as many of the graphs have vertices with an extremely high degree. From Figure 6, we see that the ML graph has nearly no edges associated with small degree vertices. Thus, with the Merge optimization many requests can be merged to 128-bytes for the ML graph. The other graphs, like...
FS, have some edges associated with small degree vertices. Thus not all of their requests can be merged. Because most vertices have long neighbor lists in the ML graph, the Merged + Aligned optimization further maximizes the 128-byte zero-copy accesses, as shown in Figure 5, and, as a result, reduces the total number of zero-copy memory requests by 28.8%, as shown in Figure 7.

To understand why the request size distribution of GK and GU graphs are significantly different for the Merged + Aligned optimization, we need to understand the neighbor list size distributions of these graphs. The neighbor lists of the GK graph are extremely unbalanced while the GU graph has uniformly low degrees varying from 16 to 48. If we assume the starting location of each neighbor list is uniformly random, then the chance of each neighbor list starting at the exact 128-byte boundary is only 6.25% when the data type size is 8-bytes. Therefore, in most cases, the neighbor lists of graphs are not aligned at the 128-byte boundary by default. If the neighbor list sizes are extremely unbalanced, like in GK, then the misalignment is less problematic since the vertices with high degrees can amortize the cost of the one-time misalignment fix. However, if all vertices have uniformly low degrees, like in GU, then there is no opportunity to amortize the cost of the one-time misalignment fix per vertex. Due to this, among all the graphs evaluated, only GU shows very little improvement with the Merged + Aligned optimization.

5.3.2 PCIe Bandwidth Analysis: The bandwidths we measured are more or less aligned with PCIe request size distributions. In Figure 8, we show the average achieved PCIe bandwidth while executing BFS. We measured the maximum achievable PCIe bandwidth with cudaMemcpy() to be 12.3GB/s. Because of the page faulting overhead present in the UVM, it can only achieve PCIe bandwidth of 9GB/s. EMOGI’s Naïve implementation of BFS can only reach up to 4.7GB/s PCIe bandwidth. This is in sync with what we observed using the toy example in Figure 4. With the merge optimization, the PCIe bandwidth utilization increased up to 11GB/s, reaching about 90% of the peak cudaMemcpy() bandwidth. With the Merged + Aligned optimization, we add about 0.5 to 1GB/s of additional bandwidth utilization on top of merge optimization in all cases. The GU graph has the least amount of improvement from the alignment optimization among all graphs. This is because BFS on the GU graph cannot send enough number of 128-byte requests to saturate PCIe interconnect bandwidth. By comparing Figure 5 and Figure 8, we can clearly see the correlation between the distribution of PCIe request sizes and the achieved bandwidths in a real application, thus confirming our the analysis in § 3.3.

5.3.3 Analysis of Zero-copy Optimizations: We next evaluate the performance difference between Naïve, Merge and Merged + Aligned implementation of BFS on various graphs and compare it with the UVM implementation. As shown in the Figure 9, the Naïve implementation’s performance is 0.73× of that of UVM on average. As discussed in § 3.3, this is expected as the Naïve implementation does not use the PCIe bandwidth efficiently. On the other hand, merging requests that go to zero-copy memory with the Merged implementation provides a speedup of 3.24× over the UVM baseline on average. For the SK graph, the performance gain using the Merged optimization is only 1.21× over UVM. This is because the SK graph can almost fit in the 16GB GPU memory. When we add memory access alignment optimization on top of merging of request with the Merged + Aligned implementation, we notice a 1.10× improvement in performance over the Merged implementation on average. This improvement can be associated with the reduced number of PCIe requests that go out to the zero-copy memory because of the Merged + Aligned optimization, as was shown in Figure 7.

5.3.4 I/O Read Amplification: We now demonstrate the I/O read amplification benefit of EMOGI’s fine-granular data accesses over the 4KB page movement in UVM in BFS graph traversal. For this experiment, we chose the Merge + Aligned EMOGI implementation to represent EMOGI as it provides the best performance. Figure 10 shows the ratio of data read from the host memory over the dataset size while performing BFS using UVM and EMOGI on each graph. UVM generally has a very high I/O read amplification factor, up to 5.16× for the FS graph, as for these graphs, the neighbor lists accessed during traversal are in different locations in memory and thus there is very little spatial locality exploited for each 4KB page moved. However, the two notable exceptions to this are the ML and SK graphs as UVM’s I/O read amplification factor for them is 2.28× and 1.14×, respectively. This is because the average degree of a vertex in the ML graph is 222 and the SK graph is so small that it can almost fit in GPU memory, thus making UVM’s page
movements a little more efficient in both cases. In contrast, EMOGI’s I/O read amplification factor doesn’t exceed 1.31x. This is because the fine-granular, merged, and aligned data access to zero-copy memory allow EMOGI to efficiently move only the necessary bytes over the slow PCIe interconnect.

5.4 Beyond BFS

In this section, we apply EMOGI’s optimization techniques to other graph traversal applications and measure their execution time. In addition to BFS from the previous sections, we add the single-source shortest path (SSSP) and connected components (CC) applications. We do not evaluate the performance with the SK and UK5 graph with CC as these graphs are directed. The overall performance results are shown in Figure 11.

EMOGI provides the best performance for all the graph traversal applications and graph datasets we studied. On average, EMOGI is 2.92x faster than UVM. For CC graph traversal application, EMOGI shows relatively lower speed-ups over UVM than the other applications. In the case of SSSP and BFS, a specific vertex is selected as a root vertex and the applications start traversing the entire graph from the root vertex. However, with CC, instead of picking a specific vertex to start with, all vertices are set as root vertices and the entire edge list is traversed. In this case, the application data access pattern is similar to streaming the edge list resulting in having more spatial locality when compared to the other applications and less I/O read amplification on the part of UVM.

5.5 Performance Scaling with PCIe 4.0

As was shown in § 5.3.2 and § 5.3.3, EMOGI can nearly saturate the PCIe 3.0 bandwidth while out-performing the UVM implementation. NVIDIA’s latest GPU, the Ampere A100, communicates with the host memory over the PCIe 4.0 interconnect. PCIe 4.0’s measured peak bandwidth, approximately 24GB/s, is twice as much as PCIe 3.0’s peak measured bandwidth of approximately 12GB/s. In this section, we study the ability of both UVM and EMOGI to take advantage of the increased bandwidth in accessing the host memory. To this end, we use a DGX A100 machine [6] with the A100 GPU and Dual AMD Rome 7742 CPUs paired with 1TB of system memory. This machine allows us to switch the root port to run in either PCIe 3.0 mode or PCIe 4.0 mode. Neither the EMOGI implementation nor the UVM implementation was re-optimized for the A100 GPU in these experiments.

The overall evaluation results comparing the performance of UVM and EMOGI on the DGX A100 system are shown in Figure 12. Here, we normalize the performance speed-up achieved by each configuration to the UVM implementation running on the A100 GPU with the PCIe 3.0 interconnect. While EMOGI’s performance scales by 1.9x on average with the faster interconnect, UVM’s performance scales by only 1.53x on average. This is because the UVM implementation suffers from page fault handling overhead when accessing pages of the edge list in host memory. The page fault handler is part of the UVM driver running on the CPU and can’t keep up to make use of the higher bandwidth of the PCIe 4.0 interface. However, EMOGI doesn’t suffer any page faulting overhead as the edge list is pinned in host memory, leading to EMOGI’s performance scaling almost linearly with the PCIe bandwidth.

5.6 Comparison with Previous Works

In this section, we compare EMOGI with the current state-of-the-art GPU solutions for out-of-memory graph traversals, HALO [21] and Subway [45]. HALO proposes a new CSR reordering method
Table 3: Comparison with the state-of-the-art GPU solutions for out-of-memory graph traversal works. The comparison with HALO [21] is done with a Titan Xp (12GB) and the comparison with Subway [45] is done with a Tesla V100 (16GB). We use graphs with 4-byte type when comparing Subway and EMOGI, as Subway only supports 4-byte data types.

| Work | App | Graph | Time (s) | EMOGI (s) | Speedup |
|------|-----|-------|----------|-----------|---------|
| HALO [21] | BFS | ML    | 9.54     | 4.43      | 2.15    |
|       |     | FS    | 8.27     | 2.59      | 3.19    |
|       |     | SK    | 2.17     | 1.62      | 1.34    |
|       |     | UK5   | 6.03     | 4.00      | 1.51    |
| Subway [45] | SSSP | GK    | 20.96    | 7.94      | 2.64    |
|       |     | FS    | 14.95    | 6.97      | 2.14    |
|       |     | SK    | 8.99     | 3.92      | 2.30    |
|       |     | UK5   | 25.78    | 8.08      | 3.19    |
|       | BFS | GK    | 6.88     | 1.66      | 4.14    |
|       |     | FS    | 4.22     | 1.49      | 2.83    |
|       |     | SK    | 1.69     | 0.85      | 1.99    |
|       |     | UK5   | 8.75     | 1.85      | 4.73    |
|       | CC  | GK    | 6.34     | 3.11      | 2.04    |
|       |     | FS    | 4.31     | 2.75      | 1.57    |

that targets improvements in data locality and data transfer during graph traversal with UVM. Subway proposes an improved design of graph partitioning that does pre-processing to determine the activeness of a vertex. Since the source code of the HALO is not publicly available, we compare EMOGI with the results available in the published paper. As HALO’s results were gathered using a Titan Xp GPU, we also use a Titan Xp instead of V100 for a fair comparison and re-measure our execution times. For Subway, we use the publicly available source code and evaluate it in our measurements. The publicly available implementation of Subway-async shows better performance than Subway-sync implementations, Subway-async shows better performance and therefore we use Subway-async to compare with our work. Since one of the goals of EMOGI is to avoid any data manipulation, we include the sub-graph generation and kernel execution time in our measurements. The publicly available implementation of Subway fails to execute on the GU graph due to unidentified CUDA out-of-memory errors and it cannot execute on the ML graph as the framework currently supports a maximum of 232 edges. Since Subway uses 4-byte data type in the edge list, we re-evaluate EMOGI with the same edge list for a fair comparison. The overall results with HALO and Subway are shown in the Table 3. Overall, across all the graph datasets and graph traversal algorithms, EMOGI observes speedups of 1.34× to 4.73× over the current state-of-the-art GPU solutions for out-of-memory graph traversals.

6 DISCUSSION

EMOGI is mainly focusing on improving the data transfer efficiency between the host memory and the GPU while traversing very large graphs. On top of EMOGI, several graph traversal specific optimizations such as a workload balancing between long and short neighbor lists [38, 39] can be added. However, it is important to understand many of the previous graph traversal specific optimizations techniques were introduced in the context of where the input graphs were small. If any of the optimizations need to increase the input dataset size by any means, they may not be suitable for out-of-memory graph traversals. For example, CuSha [31] greatly improves the chance of coalescing memory accesses for various kinds of input graphs by transforming CSR into shards, but the shards also require about 2.5× more space of CSR. The input dataset size increase in out-of-memory graph traversal is fatal since the workload is nearly entirely bottlenecked by the external interconnect bandwidth. Furthermore, the larger input dataset can be problematic for the host memory capacity as well.

On the other hand, EMOGI can potentially directly benefit from compression of input data. As discussed in § 4.3.1, many of the GPU threads are idling while waiting for the data from the host memory. While maintaining the basic structure of CSR, if each neighbor list can be stored into the host memory in a compressed form, these idling resources can be utilized to decompress the list without any overall performance loss. However, of course, such an approach requires data pre-processing and therefore a careful evaluation must be done to understand the overall improvement.

7 RELATED WORKS

Graph Analytics on GPU: Graph traversal algorithms such as BFS exhibit a massive amount of parallelism. This has led to increasing research in leveraging the massive computation power offered by GPUs to speed up graph analytics. Prior work focused on improving the performance of graph traversal algorithms either by making GPU specific algorithmic improvements [18, 28, 31, 36, 50, 53, 55] or by performing data transformations [39, 40]. However, most of these works assume graphs fit in the GPU memory.

Practical graphs, on the other hand, often cannot fit into the GPU memory. Web graphs [13, 14], social network graphs [52] and biomedical graphs [10] can be significantly larger than available GPU memory (see Table 2). To address this, prior works have proposed either to partition the input graph and loading only those edges that are needed during computation [24, 45, 47, 50] or leveraging automatic memory oversubscription using UVM [17, 21, 23, 32, 33, 35, 42]. For example, GraphReduce [47] partitions the oversized graphs and does explicit memory management between the GPU and the host memory. Recently, Subway [45] further improved the design of the input partitioning scheme using GPU-accelerated subgraph generation preprocessing that tracks activeness of a vertex and also by generating subgraphs asynchronously. EMOGI does not perform any explicit memory management or preprocessing of the graph.

Alternatively, to support large graphs in GPU, programmers can use UVM which does automatic memory oversubscription [1, 2]. Prior works such as [8, 9, 17, 21, 23, 29, 32, 33, 35, 42] have observed significant overhead from UVM and have proposed optimizations such as overlapping IO and computation [23], memory spaces [17], memory throttling [33], modifying driver to support larger page fault batch sizes [32] and reordering of graphs to enhance locality in UVM [21]. Instead of leveraging the previously proposed optimizations, EMOGI takes a step back and revisits the reasoning behind the performance degradation with UVM. Like [54], EMOGI initially

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observes the PCIe bandwidth utilization being low for graph traversal applications. As shown in § 5, by carefully re-orchestrating the memory access pattern using direct access, EMOGI is able to boost graph traversal execution performance for large graphs without any additional optimizations. Indeed the prior proposed software and hardware optimizations can be exploited by EMOGI. We leave this as future research. Also, EMOGI could be easily incorporated into a library to lessen the programmer’s effort and provide out-of-the-box performance improvements.

Multi-GPU and Collaborative CPU-GPU: Aside from single GPU graph traversal, prior works have proposed using multi-GPU [30, 41, 50, 55] and collaborative CPU-GPU computation to meet the needs of large graphs computation [22, 23, 34, 35, 49]. Multi-GPU and collaborative CPU-GPU computing are enabling using UVM where hardware moves the pages on-demand across different computing blocks. EMOGI can be extended to support both multi-GPU and hybrid CPU-GPU computing and we leave it as future research.

Architectural support for improving UVM: Besides algorithm and system-level changes, prior works also propose hardware changes that can enable executing graph traversal algorithms efficiently on large graphs. Specifically, memory compression techniques to reduce the memory footprint in the GPU [33], efficient migration policies using hardware counters, and optimized prefetching schemes [8, 9, 19], and software-hardware co-design using memory hints are proposed [2, 5]. These techniques are orthogonal to EMOGI and can be leveraged by EMOGI to gain further performance improvements in future GPU architectures.

8 CONCLUSION

In this work, we present EMOGI, a new method for optimizing the traversal of very large graphs with a GPU using zero-copy. Using a thorough analysis of fine-grained GPU memory access patterns over PCIe to zero-copy memory, we identified key optimizations to best utilize bandwidth to zero-copy memory: merged and aligned memory accesses. We applied these optimizations to key graph traversal applications to enable efficient GPU traversal of graphs that do not fit in GPU memory. Our experiments show that EMOGI out-performs the state-of-the-art solutions for traversing large graphs. This is because EMOGI avoids I/O read amplification by leveraging efficient fine-grained accesses to fetch only the needed bytes from zero-copy memory. Furthermore, EMOGI’s performance scales almost linearly with the improved bandwidth of newer interconnects as it is not bottle-necked by the page fault handling overhead of traditional methods using UVM.

ACKNOWLEDGMENTS

This work was partially supported by the Applications Driving Architectures (ADA) Research Center and Center for Research on Intelligent Storage and Processing-in-memory (CRISP), JUMP Centers co-sponsored by SRC and DARPA, IBM-ILLINOIS Center for Cognitive Computing Systems Research (C3SR) – a research collaboration as part of the IBM AI Horizon Network. This work would not have been possible without the generous hardware donations from Xilinx and NVIDIA.

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