Important Influence of Entrance Channel Reorientation Coupling on Proton Stripping

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Abstract While it is well established that the ground state reorientation coupling can have a significant influence on the elastic scattering of deformed nuclei, the effect of such couplings on transfer channels has been much less well investigated. In this letter we demonstrate that the \textsuperscript{208}Pb\left(\textsuperscript{7}Li,\textsuperscript{6}He\right)\textsuperscript{209}Bi proton stripping reaction at an incident energy of 52 MeV can be well described by the inclusion of the \textsuperscript{7}Li ground state reorientation coupling within the coupled channels Born approximation formalism. Full finite-range distorted wave Born approximation calculations were previously found to be unable to describe these data. Addition of coupling to the 0.478-MeV \(\frac{1}{2}^-\) excited state of \textsuperscript{7}Li, together with the associated two-step transfer path, has little or no influence on the shape of the angular distributions (except that for stripping leading to the 1.61-MeV \(\frac{3}{2}^+\) level of \textsuperscript{209}Bi which is significantly improved) but does affect appreciably the values of the \textsuperscript{209}Bi \(\rightarrow\textsuperscript{208}Pb + p\) spectroscopic factors. Implications for experiments with weakly-bound light radioactive beams are discussed.

While the distorted wave Born approximation in its full finite-range version (FR-DWBA) has been applied to the analysis of a wide body of heavy-ion reaction data with considerable success, it has been known since the early 1970s that certain classes of reaction, in particular (but by no means restricted to) single-proton transfers, cannot be satisfactorily described using it without recourse to such undesirable expedients as \textit{ad hoc} adjustments of the exit channel optical potential parameters. These adjustments are usually such that the resulting parameters no longer describe the relevant elastic scattering, thus violating one of the fundamental tenets of the DWBA. Many of these reactions are poorly matched, either in terms of Q value or transferred angular momentum, and at the time this led to the conjecture that the inclusion of two-step reaction paths via excited states of the projectile and/or ejectile within the coupled channels Born approximation (CCBA) formalism would enable good descriptions to be obtained without the need arbitrarily to modify the exit channel distorting potentials. However, the prohibitive computational overhead of such calculations with then available resources precluded the testing of this hypothesis.

There the question has remained in many cases for the intervening four decades as interest in heavy-ion reactions waned. However, with the advent of radioactive beams of sufficient intensity and optical quality there has been a resurgence in this field and it seems timely to revisit some of the stable beam data with a view to establishing whether they can, in fact, be satisfactorily described by including likely two-step reaction paths. Current easy availability of significant computing power makes the routine application of the full arsenal of direct reaction theory to the interpretation of such data a practical possibility. In a recent article [1] we showed that data [2,3] for the \textsuperscript{208}Pb\left(\textsuperscript{12}C,\textsuperscript{11}B\right)\textsuperscript{209}Bi single-proton stripping reaction which the FR-DWBA failed to explain could be well described by CCBA calculations including two-step transfer via the 4.44-MeV \(\frac{3}{2}^+\) excited state of \textsuperscript{12}C using shell model spectroscopic amplitudes for the projectile-like overlaps and distorting potentials that fitted the relevant elastic scattering data in both entrance and exit channels. Similar calculations for the \textsuperscript{208}Pb\left(\textsuperscript{12}C,\textsuperscript{13}C\right)\textsuperscript{207}Pb single-neutron pickup improved the already good description of the corresponding data [2,3] by the FR-DWBA.

Here we show that the 52-MeV \textsuperscript{208}Pb\left(\textsuperscript{7}Li,\textsuperscript{6}He\right)\textsuperscript{209}Bi single-proton stripping data of Zeller et al. [4], which the FR-DWBA also failed to describe satisfactorily, may be fitted simply by including the ground state reorientation coupling of the \textsuperscript{7}Li projectile, provided the description of the entrance channel elastic scattering data is maintained when the coupling is included. While the influence of ground state
reorientation coupling on the elastic scattering and excited state reorientation couplings on the inelastic scattering is well established (see, e.g., [5] and [6]), we are not aware of any previous studies that have demonstrated a significant effect of entrance channel ground state reorientation coupling on transfer channels. Addition of the excitation of the 1/2\(^-\) first excited state of \(^7\)Li and the two-step transfer path via this state produces a barely perceptible improvement in the description of the stripping data, with the exception of that for the 1.61-MeV 13/2\(^+\) level of \(^{209}\)Bi which exhibits a significant further improvement when this coupling is included. We discuss some of the implications of these results for experiments involving weakly-bound light radioactive beams.

All calculations were carried out with the code FRESCO [7]. Inputs to the CCBA calculations were kept as similar as possible to those of the original FR-DWBA calculations of Ref. [4], with the exception that the spectroscopic amplitudes for the \(^7\)Li\(^6\)He\(+\)p) overlaps were taken from [8] rather than Cohen and Kurath [9] in order to have a consistent set for all the overlaps required. However, the spectroscopic amplitudes of Refs. [8] and [9] for the \(^7\)Li(3/2\(^-\)) \rightarrow \(^2\)He(0\(^+\)) \(+\) p transition only differ by about 4%. The \(^6\)He\(+\)p and \(^{208}\)Pb\(+\)p binding potentials were as in Ref. [4]. We also retained the exit channel \(^6\)He \(+\) \(^{209}\)Bi optical potential of Ref. [4]. While this was obtained from a fit to \(^6\)Li \(+\) \(^{209}\)Bi elastic scattering data at the appropriate energy, the comparative study of Ref. [10] suggests that for incident energies this far above the Coulomb barrier \(^6\)He elastic scattering should be adequately described by \(^6\)Li optical potential parameters, even for heavy targets like \(^{209}\)Bi. Coupled discretised continuum calculations (CDCC) calculations using the modified dineutron model of Moro et al. [11] confirmed this, since the calculated elastic scattering angular distribution was well described by the exit channel potential parameters of Ref. [4].

The \(^7\)Li couplings in the entrance partition were included using standard rotational model form factors with the nuclear multipoles calculated by numerically deforming the radii of a prolate K = 1/2 band, with the Coulomb coupling strength \(B(E2; 3/2^- \rightarrow 1/2^-) = 8.3 \pm 0.5\) e\(^2\)fm\(^4\) taken from Ref. [12] and the nuclear deformation length \(\delta_2 = 2.0\) fm from Ref. [13]. Two CCBA calculations were carried out, the first including the \(^7\)Li ground state reorientation coupling only and the second the ground state reorientation plus excitation of the 1/2\(^-\) state together with the two-step transfer path via this state. In both cases the optical potential parameters were readjusted to recover the fit to the \(^7\)Li \(+\) \(^{208}\) Pb elastic scattering data of Ref. [4] and the resulting values are listed in Table 1 as sets B and C respectively, together with the original parameters of Ref. [4] (set A) for ease of reference.

The relevant coupling schemes are presented schematically in Fig. 1.

All calculations used the post form of the DWBA and included the full complex remnant term.

In Figs. 2, 3 and 4 we compare the results of FR-DWBA calculations with the data of Ref. [4].

While the data for stripping to the 0.0-MeV 9/2\(^-\) and 3.12-MeV 3/2\(^-\) levels are reasonably well described the calculations for the other levels show significant shifts in the position of the peak to larger angles compared with the data. This is particularly striking in the case of the 1.61-MeV 13/2\(^+\) level, analysis of which was not pursued in Ref. [4] due to the prohibitive computing time required with the then available resources.

Figures 2, 3 and 4 also compare the stripping data with the results of CCBA calculations including the \(^7\)Li ground state reorientation only (dashed curves) and ground state reorientation plus excitation of the 0.478-MeV 1/2\(^-\) excited state (solid curves), the latter also including the two-step transfer path via the 1/2\(^-\) excited state. Simply including the \(^7\)Li ground state reorientation coupling enables a good description of all the data, with the exception of that for stripping to the 13/2\(^+\)
Fig. 2 The $^{208}\text{Pb}(^{7}\text{Li},^{6}\text{He})^{209}\text{Bi}$ single-proton stripping data of Ref. [4] for transitions populating the 0.0-MeV 9/2$^-$ (a) and 0.90-MeV 7/2$^-$ (b) levels of $^{209}\text{Bi}$ (solid circles) compared with the results of FR-DWBA calculations (dotted curves), CCBA calculations including the $^{7}\text{Li}$ ground state reorientation coupling only (dashed curves) and ground state reorientation plus excitation of the 0.478-MeV 1/2$^-$ state (solid curves). The latter also include the two-step transfer via the $^{7}\text{Li}$ excited state.

Fig. 3 As for Fig. 2 but for transitions populating the 1.61-MeV 13/2$^+$ (a) and 2.82-MeV 5/2$^-$ (b) levels of $^{209}\text{Bi}$.

level of $^{209}\text{Bi}$ which, while considerably improved, could be better. Addition of the coupling to the 0.478-MeV 1/2$^-$ state and the associated two-step transfer path further improves the description of this level, with a relatively minor influence on the description of the other levels. Note that the good description of the stripping data by the CCBA calculations is conditional on the refitting of the entrance channel elastic scattering data with the relevant $^{7}\text{Li}$ couplings included. While the extraction of spectroscopic factors is not the goal of this work, we also note that in addition to improving the description of the angular distributions the inclusion of the ground state reorientation coupling alone and the reorientation plus inelastic excitation couplings (together with the relevant two-step transfer path) both have a significant effect on the extracted values of the spectroscopic factors for the $(^{209}\text{Bi} | ^{208}\text{Pb} + p)$ overlaps, see Table 2.

It has long been known that the ground state reorientation coupling has an important influence on the analysing powers in reactions induced by polarised beams of $^{7}\text{Li}$, the elastic scattering second-rank tensor analysing powers in particular being mainly due to this coupling. It has also been demonstrated to have a significant effect on the elastic scattering differential cross section angular distribution [5]. However, in this work we present a case where the reorientation coupling alone has an important influence on a transfer channel; in previous work of this type the $^{7}\text{Li}$ ground state reorientation has usually been associated with coupling to the 0.478-MeV 1/2$^-$ excited state, so that although significant effects on transfer reaction angular distributions were observed, the contribution of the reorientation coupling alone was not established.

We conclude with a number of observations concerning the results of this study and their bearing on the analysis of transfer reactions induced by radioactive ion beams. We have...
Table 2 Spectroscopic factors ($C^2S$) for the ($^{209}$Bi | $^{208}$Pb + p) overlap extracted from the FR-DWBA (set A) and CCBA calculations including the $^7$Li ground state reorientation coupling only (set B) and ground state reorientation plus excitation of the 0.478-MeV 1/2$^-$ excited state together with the relevant two-step transfer path (set C)

| Set | 0.0-MeV | 0.90-MeV | 1.61-MeV | 2.82-MeV | 3.12-MeV | 3.64-MeV |
|-----|--------|--------|--------|--------|--------|--------|
|     | 9/2$^-$ | 7/2$^-$ | 13/2$^+$ | 5/2$^-$ | 3/2$^-$ | 1/2$^-$ |
| A   | 1.40   | 1.19   | 0.81   | 1.07   | 0.89   | 0.64   |
| B   | 1.51   | 1.31   | 0.88   | 1.15   | 1.09   | 0.73   |
| C   | 1.68   | 1.55   | 0.98   | 1.39   | 1.34   | 0.90   |

It is also clear from Table 2 that inclusion of both ground state reorientation and excitation of the 0.478-MeV 1/2$^-$ state of $^7$Li has a significant effect on the $^{208}$Pb($^7$Li,$^6$He)$^{209}$Bi single-proton stripping data of Ref. [4] which FR-DWBA calculations were unable to fit. Addition of coupling to the 0.478-MeV 1/2$^-$ state of $^7$Li plus the corresponding two-step transfer path had only a minor effect on the shapes of the angular distributions, except for that leading to the 1.61-MeV 13/2$^+$ level of $^{209}$Bi, but did have a significant impact on the $^{209}$Bi → $^{208}$Pb + p spectroscopic factors. A good description of the elastic scattering was necessary to obtain the good fit to the stripping data. Since many weakly-bound light radioactive nuclei have similar properties, these results strongly suggest that such couplings should be included in analyses of transfer data obtained with beams of these nuclei if erroneous conclusions are not to be drawn. They also underline the need to obtain as complete a data set as possible – ideally elastic and inelastic scattering as well as the transfer process(es) of interest – to facilitate the correct inclusion of such couplings.

Data Availability Statement This manuscript has no associated data or the data will not be deposited. [Authors’ comment: The data are taken from Ref. [4].]
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