Research Article

First-Principles Study of Structure, Elastic Properties, and Thermal Conductivity of Monolayer Calcium Hydrobromide

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1. Introduction

Graphene's discovery broke the prediction that two-dimensional (2D) crystalline materials could not exist stably at finite temperatures [1–6]. Various 2D materials are limited in 2D plane because of carrier migration and heat diffusion. It has made the materials exhibit many strange properties and has attracted extensive attention [7–11]. In recent years, some scholars began to pay attention to the monolayer calcium hydrobromide (CaHBr) [12–14], which can be prepared by melting hydride with anhydrous bromide or metal with bromide in a hydrogen atmosphere at 900°C [14]. In 1996, de Castro Vítores et al. [12] obtained the bond energy of Ca-HBr complex from independent cross molecular beam and van der Waals spectroscopy experiments. Very recently, Kumar et al. [15] measured the molar heat capacities of bulk CaHBr via the differential scanning calorimetry. It can be seen that some properties of bulk CaHBr have been studied in experiments, but there are few theoretical studies on them, especially the thermal transport properties of monolayer CaHBr.

The monolayer CaHBr is a nonmagnetic wideband gap semiconductor whose heat carriers are electrons and phonons, in which phonons dominate the heat transfer. The

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lattice thermal conductivity is a key parameter for the thermal transport of semiconductors and insulators [16–19]. Peierls proposed the lattice thermal conductivity of semiconductors [20] and insulators could be described at the micro level using the phonon Boltzmann transport equation (BTE) [21]. Since then, many methods have been found to calculate the thermal conductivity of materials, such as relaxation time approximation (RTA) [22] and Callaway’s model [23, 24], where RTA contradicts inelastic scattering processes in principle, and the required parameters in the Callway model can only be obtained by fitting the experimental data [25]. Therefore, these methods have corresponding limitations.

As is known, ShengBTE code [26] can be used to obtain the crystal lattice thermal conductivity by solving the Boltzmann transport equation based on the force constants between harmonic and anharmonic atoms calculated from the first-principles [27]. To date, ShengBTE code has been successful to obtain the thermal conductivity and related physical quantities of many materials [28–33]. In this work, we will use the ShengBTE code to calculate the thermal conductivity of monolayer CaHBr, hoping to provide the reference value for the future experiments and theories.

2. Theoretical Methods and Calculation Details

The crystal structure is optimized by using the Vienna Ab initio Simulation Package (VASP) [34, 35] based on density functional theory. The Perdew–Burke–Ernzerhof (PBE) functional under the generalized gradient approximation (GGA) is selected as the exchange correlation functional [36, 37]. In order to eliminate the layer to layer interaction, we use a 25.32 Å vacuum layer. We use the cutoff energy of the plane wave to be 600 eV, the energy convergence of the electron relaxation to $10^{-6}$ eV, and a $8 \times 8 \times 1$ Monkhorst–Pack grid of k-point sampling for structural optimization. The optimized unit lattice is expanded to a supercell of $3 \times 3 \times 1$, and then, the second-order harmonic force constants (harmonic IFCs) and the third-order anharmonic force constants (anharmonic IFCs) are calculated by using Phonopy software and ShengBTE, respectively. And using the Phonopy software package can also get the phonon frequency.

There have been many studies detailing the calculation of lattice thermal conductivity using ShengBTE code [25, 26, 30, 31]; so here, we just briefly introduce this method. The resulting linearized phonon BTE when the scattering source is only two-phonon and three-phonon processes can be written as

$$F_{\lambda} = \tau_{\lambda}^{0} (\omega_{\lambda} + \Delta_{\lambda}),$$

where $\tau_{\lambda}^{0}$ is the relaxation time of mode $\lambda$, as obtained from perturbation theory. As a matter of fact, setting all $\Delta_{\lambda}$ to zero is equivalent to working within the RTA. The three-phonon scattering rates can be expressed as $\omega_{j} (q) + \omega_{j} (q') = \omega_{j} (q'')$, where $\omega_{j} (q)$ is the phonon frequency of mode $j$, $q$ is normal process correspond to $G = 0$, while Umklapp processes correspond to $G \neq 0$.

The lattice thermal conductivity $k_{\lambda}$ can be obtained in terms of $F$ as

$$k_{\lambda}^{\beta} = \frac{1}{\kappa_{\beta} T^{2} \Omega N} \sum_{j} f_{0} (f_{0} + 1) (\hbar \omega_{j})^{2} \sigma_{j}^{\beta} F_{\lambda}^{j},$$

where $\Omega$ is the unit cell volume. In the approach implemented in ShengBTE, equation (2) is starting with a zeroth-order approximation $F_{\lambda}^{j} = \tau_{\lambda}^{0} \omega_{j}$. The stopping criterion is that the relative change in the calculated conductivity tensor is less than a configurable parameter. Stopping at the zeroth iteration is equivalent to operating under the RTA. In addition, many physical quantities can also be calculated by ShengBTE code, such as the scalar mean free path $\Lambda_{\lambda}$ for mode $\lambda$.

$$\Lambda_{\lambda} = \frac{F_{\lambda} \cdot v_{\lambda}}{|v_{\lambda}|}$$

3. Results and Discussion

3.1. Structure and Elastic Properties. The initial structure of the monolayer CaHBr is obtained from the bulk CaHBr belonging to the orthogonal structure (P4) crystal. In order to obtain the equilibrium geometric structure of monolayer CaHBr, we use the GGA method to calculate the lattice constant $a$ and obtain the total energy $E$ and the corresponding cell volume $V$; the energy-volume $(E-V)$ data are then fitted to the Vinet equation [29]. Thus, we obtain the equilibrium lattice constant $a = 3.843$ Å, which is well consistent with another theoretical value $a = 3.829$ Å [38].

The elastic constants $C_{ij}$ of materials are the critical significance physical quantity to measure the mechanical energy and important parameter to reflect the mechanical properties of materials [39–41]. Thus, the calculation of the elastic constant $C_{ij}$ is of great significance for the measurement of the elastic limit of the lattice under external stress. We can calculate the elastic constants $C_{ij}$ of two-dimensional materials by using the related theory of bulk elastic constants. In Table 1, we list the calculated elastic constants $C_{11}$, $C_{22}$, $C_{12}$, and $C_{66}$, which can be used to obtain the layer modulus $\gamma_{0}$, Young’s modulus $Y_{2D}$ under the Cavendish coordinates (its directions [10] and [01] in 2D materials), and Poisson’s ratio $\nu$ [42, 43].

$$\gamma_{0} = \frac{1}{4} (C_{11} + 2C_{22} + 2C_{12}),$$

$$Y_{2D} = Y_{01}^{2D} = \frac{C_{11}C_{12} - C_{12}^{2}}{C_{22}},$$

$$\nu_{10} = \nu_{01} = \frac{C_{12}}{C_{11}}.$$

The monolayer CaHBr satisfies the stability criterion, which can be expressed by four necessary and sufficient conditions for the determination of mechanical stability [40, 41]: $C_{11} > 0$, $C_{66}$ (the bulk material is $C_{44} > 0$,
The relationship between biaxial strains and pressures of monolayer CaHBr.

**Table 1:** Elastic constants \( C_{ij} (Nm^{-1}) \) and shear modulus \( G^{2D} \), layer modulus \( Y_0 \), Young’s modulus \( Y^{2D} \), Poisson’s ratio \( \nu \), the ratio of layer modulus, and shear modulus \( (\nu_0/G^{2D}) \) for the monolayer CaHBr.

| Elastic properties | Our results |
|--------------------|-------------|
| \( C_{11} \)      | 64.11       |
| \( C_{22} \)      | 64.11       |
| \( C_{12} \)      | 5.23        |
| \( C_{66} = G^{2D} \) | 17.98       |
| \( \nu \) \( Nm^{-1} \) | 34.67       |
| \( Y^{2D} \) \( Nm^{-1} \) \( = Y^{2D}_{[01]} \) | 63.69       |
| \( \nu_0 = \nu_{[01]} \) | 0.082       |
| \( \nu_0/G^{2D} \) | 1.928       |

In Figure 3, we illustrate the contributions of the phonon modes to total lattice thermal conductivity at room temperature. The phonon acoustic branches clearly dominate the lattice thermal conductivity of the monolayer CaHBr, while the contribution from the optical branches is quite small. Although the contribution of the optical branch is small, the optical branch provides a scattering channel for the acoustic mode, resulting in the three-phonon scattering. So, the contribution of the optical branches cannot be ignored [29, 48].

The total converged phonon scattering rates of the monolayer CaHBr at room temperature are illustrated in Figures 4 and 5, which are corresponding to the acoustic modes and the optic modes, respectively. We notice that there is a gap between the acoustic and optical branches, consistent with that of the phonon spectra in Figure 2(a). The phonon scattering rate of the three acoustic branches is much smaller than that of the optical branch, from which it can be seen that the acoustic branch mainly contributes to the thermal conductivity of this material.

**3.3. Phonon Mean Free Path and Thermal Conductivity.** By calculating the phonon mean free path (MFP), we can understand how the material size affects the thermal conductivity. In Figure 6, we show the functional relationship...
between the cumulative lattice thermal conductivity and the maximum mean free path (MFP) \( \Lambda_{\text{max}} \) at room temperature. When drawing a curve with a logarithmic scale as the horizontal axis, we can find the similarity of the curve to a logistic function, indicating that the form is suitable for the following nonparametric function:

\[
\kappa_{\text{i}}(\Lambda \leq \Lambda_{\text{max}}) = \frac{\kappa_{\text{i}}}{1 + (\Lambda_0/\Lambda_{\text{max}})}. \tag{7}
\]

It is found from Figure 6 that the acoustic phonons with a length of 0–3.5 nm contribute to the thermal conductivity, while the optical phonons larger than 3.5 nm contribute little to the thermal conductivity.

For the efficiency and reliability of devices, the thermal transport property of materials is very important. At present, there are no experimental data and theoretical data for the thermal conductivity of the monolayer CaHBr. By testing the sensitivity of the thermal conductivity to the temperature, the functional relationship between the lattice thermal conductivity and the temperature can be obtained in Figure 7, where we show the lattice thermal conductivities \( \kappa_{\text{i}} \) of the monolayer CaHBr in the temperatures ranging from

![Figure 2: (a) The calculated phonon dispersion curves of monolayer CaHBr. (b) and (c) Main view and side view of primitive unit cell of monolayer CaHBr.](image1.png)

![Figure 3: Contributions of phonon modes to total lattice thermal conductivity, where the red bars represent the ZA branches of acoustics, the green bars represent the TA branches of acoustics, the blue bars represent the LA branches of acoustics, and the orange bars represent the optical branches.](image2.png)
30K to 1200K with a $94 \times 94 \times 1$ k-grid in the scalebroad $= 1.0$. It can be seen that the lattice thermal conductivity increases exponentially with the increase of temperature $T$ at low temperatures and tends to be proportional to $1/T$ at high temperatures. The lattice thermal conductivity of monolayer CaHBr at room temperature is 2.469 W/m·K and 2.201 W/m·K for BTE and RTA, respectively.

**Figure 4:** The phonon scattering rates of monolayer CaHBr at room temperature. The red squares (ZA), green triangles (TA), and blue circles (LA) are the acoustic modes.

**Figure 5:** The phonon scattering rates of monolayer CaHBr at room temperature. The orange star is for the optic modes.

**Figure 6:** Calculated cumulative thermal conductivity of monolayer CaHBr as a function of maximum mean free path (MFP) at room temperature.

**Figure 7:** Lattice thermal conductivity $\kappa$ of monolayer CaHBr at different temperatures ranging from 30 K to 1200 K. Black squares, our results from RTA; red circles, our results from iterative solution of BTE with scalebroad $= 1.0$.

### 4. Conclusions

Based on density functional theory and Boltzmann transport equation, we study the structure, elastic properties, and lattice thermal conductivity of the monolayer CaHBr. The obtained equilibrium lattice constant $a = 3.843 \text{ Å}$ is well
consistent with another theoretical value $a = 3.829 \, \text{Å}$. The mechanical and thermodynamic stability of monolayer CaHBr is proved by the obtained elastic properties and phonon spectra without imaginary frequency. And the elastic limit of monolayer CaHBr is obtained by biaxial tensile strain. The second-order and third-order interatomic force constants are obtained by using the finite difference method. The thermal conductivity of the monolayer CaHBr at room temperature is $2.469 \, \text{W/m} \cdot \text{K}$ and $2.201 \, \text{W/m} \cdot \text{K}$, respectively, by BTE and RTA iterations. The two methods can obtain good results for the calculation of thermal conductivity of monolayer CaHBr. It can be seen that the lattice thermal conductivity of the obtained monolayer CaHBr is low, and the result shows that the lattice thermal conductivity mainly depends on the acoustic modes. We hope that our results can provide theoretical guidance for the experimental exploration and application of the relevant properties of layered monolayer CaHBr.

Data Availability

The data used to support the findings of this study are included within the article.

Conflicts of Interest

The authors declare that they have no known conflicts of interest.

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