Constraints on Scalar Field Dark Matter from Colocated Michelson Interferometers

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Low-mass scalar field dark matter may induce apparent oscillations of fundamental constants, resulting in corresponding oscillations of the size and the index of refraction of solids. Laser interferometers are highly sensitive to changes in the size and index of refraction of the main beam splitter. Using cross-correlated data of the Fermilab Holometer instrument, which consists of twin colocated 40-m arm length power-recycled interferometers, we investigate the possible existence of scalar field dark matter candidates in the mass range between $1.6 \times 10^{-12}$ eV and $1.0 \times 10^{-7}$ eV. We set new upper limits for the coupling parameters of scalar field dark matter, improving on limits from previous direct searches by up to 3 orders of magnitude.

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Introduction.—Cosmological modeling suggests “dark matter” (DM) comprises a large fraction of the total matter content of the universe; its origin and physical properties remain unknown to date. Although indirect astronomical observations in the last decades seem to confirm its existence, a first direct detection of dark matter is still missing and represents one of the greatest challenges of contemporary physics.

In scenarios where a low-mass scalar field constitutes DM, the field can couple to interferometric detectors, which then produces a signal. This prediction can be used to search for DM signals, and if no signal is detected, constraints on the DM parameters can be placed. Recent examples of this new type of DM search have involved gravitational wave detectors: GEO 600 [1] for scalar field DM [2,3] and Advanced LIGO and Advanced VIRGO [4,5] for dark photon DM [6]. Thanks to technological progress, these precision interferometers can now reach sensitivities to length variations at or beyond quantum limits, and they can be used in contexts different from the ones for which they were originally developed.

In this work, we perform a direct search for scalar field DM using the data of the Fermilab Holometer instrument [7,8], which consists of twin Michelson interferometers. Its cross-correlation sensitivity in the 1–25 MHz frequency range allows us to set new upper limits on the coupling parameters of scalar field dark matter in a different DM mass range from the one already constrained by the GEO 600 interferometer and other experiments.

Theory.—The work presented in this Letter concerns low-mass ($m_\phi \ll 1$ eV) DM models. In this scenario, the DM is represented by a scalar field $\phi$ of mass $m_\phi$ that couples with the standard model (SM) fields. The coupling is parameterized by the addition of an interaction term in the SM Lagrangian [3,9].

In this Letter, we only consider interactions linear in $\phi$ [1,3]; the resulting Lagrangian is of the form

$$L_{\text{int}}^{\phi \phi} = \frac{\phi^2 F_{\mu\nu} F^{\mu\nu}}{4} - \frac{\phi \bar{\psi}_e \gamma_\mu \psi_e}{\Lambda_e},$$

where $F_{\mu\nu}$ is the electromagnetic field tensor, $m_\psi$ the electron rest mass, and $\bar{\psi}_e, \psi_e$ the SM electron field and its Dirac conjugate. $\Lambda_\gamma$ and $\Lambda_e$ parameterize the coupling of the DM field with photons and electrons, respectively. Some scalar field DM models motivated by string theory, such as the modulus and dilaton fields, couple to the QCD sector of the SM as well [10,11]. These other couplings make such undiscovered massive scalars subject to additional experimental constraints, although the predicted phenomenology due to the electromagnetic coupling terms [Eq. (1)] remains unchanged. Relaxations are nondilatonic scalars that couple to the standard model by mixing with the Higgs field [12]; however, their coupling to the electromagnetic sector can be effectively described by Eq. (1) and thus relaxion DM would produce the same variation of the fundamental constants.

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For sub-eV masses, the field manifests as an oscillating classical field [2]:

$$\phi(t, \vec{r}) = \phi_0 \cos(\omega_\phi t - \vec{k}_\phi \cdot \vec{r}),$$  \hspace{1cm} (2)

where $\omega_\phi = (m_\phi c^2/\hbar)$ is the angular Compton frequency, $\vec{k}_\phi = (m_\phi v_{\text{obs}}/\hbar)$ the wave vector, and $v_{\text{obs}}$ the velocity relative to the observer. Under the assumption that the field is DM, its amplitude is given by $\phi_0 = (\hbar \sqrt{2 \rho_{\text{local}}}/m_\phi c)$ [13], where $\rho_{\text{local}}$ is the local DM density.

The presence of an oscillating DM field interacting with the SM fields makes the fundamental constants oscillate at the Compton frequency of the DM field. This causes the electron rest mass $m_e$ and the fine structure constant $\alpha$ to be altered as [2,3,9]

$$m_e \rightarrow m_e \left(1 + \frac{\phi}{\Lambda_e}\right), \quad \alpha \rightarrow \alpha \left(1 + \frac{\phi}{\Lambda_j}\right).$$  \hspace{1cm} (3)

By looking for changes of the size $l$ and the refractive index $n$ of a solid [3] caused by the oscillatory variation of $\alpha$ and $m_e$, the coupling of DM to SM fields can be probed. The response of a solid to perturbations with a particular driving frequency $\omega$ can be modeled as a driven harmonic oscillator. The amplitude of the size change of the solid is given to first order by

$$\delta l = \left(\frac{-\delta \alpha - \delta m_e}{\alpha - m_e}\right) \left(1 - \frac{\omega^2}{\omega_0^2}\right)^{-1},$$  \hspace{1cm} (4)

where $\omega_0$ is the angular frequency of the fundamental longitudinal vibrational mode of the solid driven by the scalar field, and we consider a strongly underdamped system.

The variation of the refractive index of a solid due to the interaction with the DM field is given by [3]

$$\frac{\delta n}{n} \approx -5 \times 10^{-3} \left(2 \frac{\delta \alpha}{\alpha} + \delta m_e/m_e\right).$$  \hspace{1cm} (5)

A very suitable experimental setup to investigate the presence of changes in the size and refractive index of solids is a laser interferometer. In this instrument, a dedicated optic, the beam splitter, splits the incoming laser beam into the two arms. The beam splitter has a partially reflective front surface (typically 50%) and an antireflective back surface. The light entering one arm is therefore reflected off the front surface, whereas light entering the other arm is transmitted through the beam splitter. This asymmetry causes changes in the size and refractive index of the beam splitter to generate a difference between the optical path lengths of the arms $L_x$ and $L_y$. Given the geometry of a Michelson interferometer, the resulting optical path length difference is expected to be given by [1]

$$\delta(L_x - L_y) \approx \sqrt{2} \left[\left(n - \frac{1}{2}\right) \delta l + l \delta n\right].$$  \hspace{1cm} (6)

For the current analysis, we use the data from the Fermilab Holometer experiment, which has been constructed to search for exotic quantum space-time correlations [14] (see “The Holometer experiment” below). As the spatial coherence length of light scalar field dark matter [$\lambda_\phi = 1/|k_\phi|$; see Eq. (2)] is much greater than the separation of the interferometers, possible DM signals in the two instruments would appear in phase at any time. As dominant sources of noise (i.e., photon shot noise) are incoherent between the two systems, we can take a coherent average of the cross-spectrum over time to increase the signal-to-noise ratio for potential DM signals, which then increases with the square root of the total measurement time. This yields a sensitivity orders of magnitude greater than would be obtained with a single instrument or using only the autospectrum of either interferometer. Specifically, the coherently averaged cross-spectral sensitivity lies 5 orders of magnitude below the single-instrument noise floor for the current dataset.

The magnitude of the expected signal due to scalar field dark matter in the cross-spectrum is then given by considering the optical response of the Holometer to the signal in Eq. (6), which gives

$$\delta(L_x - L_y) \approx \left(\frac{2 c L \sqrt{\rho_{\text{local}}}}{\omega_\phi c}\right) \left[\frac{\sin\left(\frac{\omega_\phi L}{c}\right)}{\omega_\phi L}\right]^{-1} \times \left\{ n - \frac{1}{2} \right\} \left(1 - \frac{\omega^2}{\omega_0^2}\right)^{-1} \left(\frac{1}{\Lambda_j} + \frac{1}{\Lambda_e}\right) + n \left(\frac{10^{-2}}{\Lambda_j} + 5 \times 10^{-3}\right) \left(\frac{1}{\Lambda_e}\right),$$  \hspace{1cm} (7)

where the sinc function describes the modulation of the signal due to the periodic frequency response of an interferometer with arms of length $L$. $\omega_0$ is the fundamental angular vibrational frequency of the beam splitter, which is $2\pi \times 226$ kHz for the Holometer [14].

The mechanical mounting of the beam splitter has a very minor effect on this resonance. A naive model of the vibrational modes of a simple cylinder, with dimensions and material matching the beam splitter, predicts a fundamental planar mode frequency of 225 kHz, whereas the measured value of the resonance is 226 kHz; i.e., the mount structure causes a frequency shift of less than 0.5%. A detailed description of this effect is reported in Section 6.5.1 of [14].

Data analysis and results.—The Holometer consists of two independent power-recycled 40-m arm length Michelson interferometers, co-aligned and separated by 0.9 m beam splitter to beam splitter. In each interferometer, continuous-wave 1064 nm laser light is injected to the beam splitter and routed along two distinct paths through the...
interferometer arms to distant end mirrors. The instrument is an overcoupled Fabry-Perot cavity whose free spectral range of 3.85 MHz is determined by the average arm length. A typical resonating power of 1.3 kW from 1 W of injected power is achieved. A separate radio frequency data acquisition system samples the interferometer output intensities at 50 MHz and computes their cross-spectral density with 25 MHz bandwidth. (A detailed description of the Holometer detector design is provided in [14].)

We performed the analysis on a 704-hr dataset acquired between July 2015 and February 2016 [7,8]. During the data taking, the photodetector signals of the two interferometers were sampled at 50 MHz. The time-series data were segmented and windowed (overlapping successive segments by 50% to preserve information [15]), after which discrete Fourier transforms (DFTs) were computed. Each DFT batch was used to compute a cross-spectrum. Finally, a coherent average over time of all cross-spectra was taken in order to reduce the noise [8,14]. (A detailed description of the data acquisition system can be found in Section 5.3 of [14]).

We then searched for significant peaks relative to the background noise in the cross-spectrum magnitude. A peak was considered a possible candidate when there was less than 5% probability that it was due to noise. This probability was determined under the assumption that the noise was Rayleigh distributed and stationary, which has been verified in previous work [16]. The median of the local noise distribution of the time-averaged cross-spectrum was estimated at each frequency bin, using a moving average over neighboring frequency bins. Different values for the number of neighboring bins in the moving window (N) were used for different frequency regions [18].

The frequency-dependent noise variance was estimated directly as the sample variance of all DFTs taken over time. The total error σ also includes a calibration error inherent to the apparatus. The look-elsewhere effect was compensated with the application of a trial factor of approximately ∼6 × 10^4 to account for the number of bins in the cross-spectrum. The performed analysis resulted in the identification of two possible candidates above the 95% confidence level (CL), i.e., > 5.31σ, as shown in Fig. 1.

These two peaks were then subjected to further analysis to investigate if either was a DM signal. Both the identified relevant peaks in the amplitude spectrum were related to known harmonic sources inherent to the experiment. The first, at ∼13 MHz, is injected for diagnostic monitoring of the readout system by a LED placed directly in front of the photodetectors. The second peak, at ∼20.5 MHz, is the radio frequency control sideband used to phase lock the lasers to the resonant interferometer cavities [17].

Having ruled out the presence of signals due to scalar field DM, we set new constraints on the DM parameters at the 95% CL using Eq. (7), applying our analysis to three different DM scenarios.

The first scenario is the “basic scalar”; see Fig. 2 (top). In this scenario, the interaction between the scalar field DM and the SM fields is fully described by Eq. (2). The scalar field is assumed to be homogeneous in the solar system and, according to the standard galactic DM halo model [13], its density is equal to ρ = 0.4 GeV/cm^3.

![Amplitude autospectrum of the single interferometers (black and green) and the cross-spectrum magnitude (blue) obtained from the Holometer’s coherently averaged data. At frequencies above ≈1 MHz the spectrum is dominated by photon shot noise; below ≈1 MHz environmental (mechanical) and laser noise dominate [14]. In particular, below 500 kHz the dominant noises are laser amplitude and phase noise—for a detailed description of their characterization, see Sections 6.4.1 and 6.4.2 of [14]. For each frequency bin, the local noise median (cyan) was estimated from its neighboring bins. The 95% CL (red) was then computed assuming the noise to be Rayleigh distributed. Peaks (red) above the 95% CL were considered possible DM candidates and were investigated further.](image-url)

FIG. 1. The amplitude autospectrum of the single interferometers (black and green) and the cross-spectrum magnitude (blue) obtained from the Holometer’s coherently averaged data. At frequencies above ≈1 MHz the spectrum is dominated by photon shot noise; below ≈1 MHz environmental (mechanical) and laser noise dominate [14]. In particular, below 500 kHz the dominant noises are laser amplitude and phase noise—for a detailed description of their characterization, see Sections 6.4.1 and 6.4.2 of [14]. For each frequency bin, the local noise median (cyan) was estimated from its neighboring bins. The 95% CL (red) was then computed assuming the noise to be Rayleigh distributed. Peaks (red) above the 95% CL were considered possible DM candidates and were investigated further.
FIG. 2. Computed constraints on the coupling parameters $\Lambda_e$ (left) and $\Lambda_\gamma$ (right) as a function of the field’s mass $m_\phi$ for scalar field DM as in the basic scalar scenario (top), the dilaton or modulus scenario (middle), and the relaxion halo scenario (bottom). Electron and photon coupling constraints are at the 95% CL. The region colored in red indicates the parameter space for the coupling parameters excluded by our analysis of the Holometer data. Other colored regions mark the parameter space excluded by other direct searches [19–21], including the AURIGA experiment [22] and the GEO 600 interferometer [1]. The gray regions denoted by the black curves are constraints on general fifth forces and tests of the equivalence principle [23]. These come from the space-based MICROSCOPE experiment [24], and the Cu-Pb and the Be-Ti torsion pendulum experiments performed by the Eöt-Wash group [25–27]. For the relaxion halo scenario, a mass-dependent DM halo density as described in [28] has been assumed. The constraints obtained for this scenario from direct experimental searches have been obtained by rescaling the original ones to account for this dependence. Constraints from fifth-force and equivalence principle tests do not depend on the local DM density and are thus the same as in the dilaton or modulus scenario.
The second scenario is the “dilaton or modulus”; see Fig. 2 (middle). The density of the DM field is assumed to be the same as in the basic scalar model. With respect to the previous scenario, the dilaton or modulus is constrained by additional limits from equivalence principle tests but is equally constrained by our results.

The third scenario is the “relaxion halo”; see Fig. 2 (bottom). Here, it is assumed that a relaxion halo gravitationally bound to Earth dominates the local DM density, and leads to a local overdensity (which depends on the field’s mass) that can reach values of up to $(\rho_{\text{local}}/\rho) \sim 10^{19}$ for the mass range constrained by our analysis [28].

The coupling between the DM scalar field and the SM field is as in the dilaton or modulus scenario (although these couplings arise through mixing with the Higgs boson).

The electron and photon coupling parameters, $\lambda_e$ and $\lambda_{\gamma}$, respectively, are constrained for each scenario as a function of the field’s mass $m_{\phi}$, assuming for each coupling parameter the other to be zero. The new constraints obtained from our analysis, together with previously published upper limits, are plotted in Fig. 2. The feature at 226 kHz is due to the mechanical resonance of the beam splitter, where the apparent depth of the minimum is limited by the frequency resolution (the $Q$ factor of the beam splitter is more than an order of magnitude greater than the plotted amplitude enhancement).

**Conclusions.** —In this Letter, we have looked for signals of scalar field DM in the cross-spectrum of colocated interferometers, which constitutes the first direct search of scalar DM using correlated interferometry.

Our analysis excluded the presence of scalar field DM signals in the data, placing lower limits on the DM coupling parameters for DM masses between $1.6 \times 10^{-12}$ eV and $1.0 \times 10^{-7}$ eV. These limits improve over previous direct experimental bounds in several subranges: we set limits in the previously unconstrained mass range between $2.4 \times 10^{-11}$ and $4.3 \times 10^{-11}$ eV, and improve over the existing constraints [21] in the mass range $8.2 \times 10^{-9} - 6.2 \times 10^{-8}$ eV by up to 3 orders of magnitude.

Constraints on the coupling parameters of scalar field DM have been previously obtained in many distinct mass ranges with different types of experiments: optical cavities [20], atomic spectroscopy [19,21], and gravitational-wave detectors like the resonant bar AURIGA [22] and the GEO 600 interferometer [1]. Finally, equivalence principle tests exploiting torsion balances [25,26] have been used to compute constraints on scalar fields under the assumption they manifest as a “fifth force” and are sourced by a test mass [24,29]. These constraints are independent of the local DM density, and depend in general on the composition and geometry of the test masses.

Better constraints on scalar field DM can be achieved through upgrades of current experiments [21], increases in the measurement time of correlated instruments, or new, more sensitive experiments (e.g., [30]).

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[1] S. M. Vermeulen, P. Relton, H. Grote, V. Raymond, C. Affeldt, F. Bergamin, A. Bish, M. Brinkmann, K. Danzmann, S. Doravari et al., Nature (London) 600, 424 (2021).

[2] Y. Stadnik and V. Flambaum, Phys. Rev. Lett. 115, 201301 (2015).

[3] H. Grote and Y. V. Stadnik, Phys. Rev. Research 1, 033187 (2019).

[4] H.-K. Guo, K. Riles, F.-W. Yang, and Y. Zhao, Commun. Phys. 2, 155 (2019).

[5] R. Abbott et al., arXiv:2105.13085.

[6] A. Pierce, K. Riles, and Y. Zhao, Phys. Rev. Lett. 121, 061102 (2018).

[7] A. S. Chou, R. Gustafson, C. Hogan, B. Kamai, O. Kwon, R. Lanza, L. McCuller, S. S. Meyer, J. Richardson, C. Stoughton et al., Phys. Rev. Lett. 117, 111102 (2016).

[8] A. Chou, H. Glass, H. Richard Gustafson, C. J. Hogan, B. L. Kamai, O. Kwon, R. Lanza, L. McCuller, S. S. Meyer, J. W. Richardson et al., Classical Quantum Gravity 34, 165005 (2017).

[9] Y. Stadnik and V. Flambaum, Phys. Rev. Lett. 114, 161301 (2015).

[10] T. Damour and A. Polyakov, Nucl. Phys. B423, 532 (1994).

[11] A. Arvanitaki, S. Dimopoulos, and K. Van Tilburg, Phys. Rev. Lett. 110, 031102 (2016).

[12] T. Flacke, C. Frugiuele, E. Fuchs, R. S. Gupta, and G. Perez, J. High Energy Phys. 06 (2017) 050.

[13] J. I. Read, J. Phys. G 41, 063101 (2014).

[14] A. Chou, H. Glass, H. Richard Gustafson, C. Hogan, B. L. Kamai, O. Kwon, R. Lanza, L. McCuller, S. S. Meyer, J. Richardson et al., Classical Quantum Gravity 34, 065005 (2017).

[15] P. Welch, IEEE Trans. Audio Electroacoust. 15, 70 (1967).

[16] The cross-spectral density magnitude is a Rayleigh-distributed quantity, as the real and imaginary parts of the cross-spectral density, taken individually, are Gaussian-distributed. The Gaussianity of the Holometer data has been previously established; see Fig. 2 of [17] and, in particular, Fig. 16 of [14].

[17] J. G. C. Martinez and B. Kamai, Classical Quantum Gravity 37, 205006 (2020).

[18] The choice of $N$ represents a trade-off between erroneously assuming instrumental spectral artifacts or signals to be
features of the underlying noise spectrum versus erroneously assuming features of the underlying noise spectrum to be instrumental spectral artifacts or signals. In other words, $N$ has to be chosen such that the autocorrelation length of the noise spectrum is much greater than $N$. We used different window sizes $N$ in five frequency regions, i.e., $N = 500$ (840 kHz–25 MHz), $N = 250$ (650–840 kHz), $N = 70$ (250–650 kHz), $N = 20$ (14–250 kHz), and $N = 4$ (381 Hz–14 kHz).

[19] S. Aharony, N. Akerman, R. Ozeri, G. Perez, I. Savoray, and R. Shaniv, Phys. Rev. D 103, 075017 (2021).
[20] E. Savalle, A. Hees, F. Frank, E. Cantin, P.-E. Pottie, B. M. Roberts, L. Cros, B. T. McAllister, and P. Wolf, Phys. Rev. Lett. 126, 051301 (2021).
[21] D. Antypas, O. Tretiak, A. Garcon, R. Ozeri, G. Perez, and D. Budker, Phys. Rev. Lett. 123, 141102 (2019).
[22] A. Branca, M. Bonaldi, M. Cerdonio, L. Conti, P. Falferi, F. Marin, R. Mezzena, A. Ortolan, G. A. Prodi, L. Taffarello et al., Phys. Rev. Lett. 118, 021302 (2017).
[23] N. Leefer, A. Gerhardus, D. Budker, V. Flambaum, and Y. Stadnik, Phys. Rev. Lett. 117, 271601 (2016).
[24] J. Bergé, P. Brax, G. Métris, M. Pernot-Borràs, P. Touboul, and J.-P. Uzan, Phys. Rev. Lett. 120, 141101 (2018).
[25] G. L. Smith, C. D. Hoyle, J. H. Gundlach, E. G. Adelberger, B. R. Heckel, and H. E. Swanson, Phys. Rev. D 61, 022001 (1999).
[26] T. A. Wagner, S. Schlamming, J. H. Gundlach, and E. G. Adelberger, Classical Quantum Gravity 29, 184002 (2012).
[27] S. Schlamming, K.-Y. Choi, T. A. Wagner, J. H. Gundlach, and E. G. Adelberger, Phys. Rev. Lett. 100, 041101 (2008).
[28] A. Banerjee, D. Budker, J. Eby, H. Kim, and G. Perez, Commun. Phys. 3, 1 (2020).
[29] A. Hees, O. Minazzoli, E. Savalle, Y. V. Stadnik, and P. Wolf, Phys. Rev. D 98, 064051 (2018).
[30] S. M. Vermeulen, L. Aiello, A. Ejlli, W. L. Griffiths, A. L. James, K. L. Dooley, and H. Grote, Classical Quantum Gravity 38, 085008 (2021).