Plasticity Autowave Characteristics of Metals and the Periodic Table of Elements

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Abstract: In this paper, the general laws of localized plastic flow development are described for the linear work hardening stages of nineteen metals. The correlations are established and discussed between their element position in the periodic table of elements and the parameters of the autowave process of localized plastic flow in these elements. Patterns of plastic flow are considered for nineteen metals from the 3rd, 4th, 5th, and 6th periods of the periodic table of elements. A conditional characteristic of plasticity is introduced and its relationship with the position of the metals in the periodic table of elements is established. Correlations between the plastic properties and other metal characteristics were analyzed. Some quantitative models are proposed for explaining the observed dependency origin by the drag of moving dislocation by electron gas in metal crystals. Observed correlations indicate the existence of a close bond between localized plastic flow in deforming medium with the lattice characteristics of the elements and their electron structures.

Keywords: metals; plasticity; autowave; crystal lattice; localization; periodic table

1. Introduction

One of the fundamental questions of physics and materials science is the prediction of the physical and chemical properties of materials based on the periodic law and the correlation of properties. Periodic changes in the values of Young’s modulus, shear modulus, bulk modulus of elasticity, and compressibility, with continuous growth of their positions in the periodic table of elements Z, are already well known [1,2]. In [3], the dependence of the work function of an electron on the atomic number of an element was constructed. A certain periodicity is observed depending on the value of the work function of the electron of metals on the atomic number. The maxima correspond to d-metals with an face-centered cubic (FCC) structure (rhodium, palladium, iridium, and platinum), while local minima are observed in the regions of niobium and rhenium. Numerous estimates of the theoretical strength of metals lead to an approximate relationship between theoretical strength and Young’s modulus and shear moduli.

It should be noted that there are no simple relationships common to all polycrystalline materials and their mechanical properties (hardness, yield strength, ultimate strength, relative elongation, elastic characteristics, shear modulus G, Young’s modulus E, and bulk modulus B). The existence of some tendencies links the elastic and plastic properties of metals, for example, according to the criterion in [1]: the higher the B/G ratio of the metal under consideration, the greater its plasticity. Information about the characteristics of elasticity and their relationship with other properties of the material sheds light on the essence of many physical and mechanical properties of the material. The elastic interaction of crystal lattice defects is a natural method for describing changes in microstructure and processes occurring in a material under load.

The problem of an adequate physical comprehension of a solid’s plasticity nature remains relevant. For progress in this area, information on the existence and form of dependencies of metals plasticity characteristics on their positions in the periodic table of elements, and with particular relevance to the strong dependence of some physical
The modern model of plasticity phenomena, developed in [5], is as follows: The spatiotemporal distributions of localized deformation nuclei, called localized plasticity patterns [6], are formed at all the work hardening stages. The pattern origin is explained by how the self-organization of the defect (dislocation) ensembles in the deforming medium by means of macroscopic deformation localization [7]. Similar patterns are projections of plastic flow autowaves, emerging at each stage of work and hardening on the surface of the test specimen. The autowaves are characterized by spatial (autowave length), $\lambda \approx 10^{-2}$ m, and temporal scales (autowave period), $T \approx 10^{-2}$ s, and propagate with velocity $10^{-5} \leq V_{aw} \leq 10^{-4}$ m/s. The product ($\lambda \cdot V_{aw}$) is referred to as the plasticity parameter and characterizes the plastic flow at a macroscopic scale level.

It is well known that the total strain is the sum of the plastic and the elastic parts. Elastic field redistribution by deformation occurs by the transverse elastic waves, with the velocity, $V_t = 2\chi\omega_D \approx 10^3$ m/s. Here, $\chi \approx 10^{-10}$ m is the interplanar spacing, $\omega_D = k_B\theta_D/\hbar \approx 10^{13}$ Hz is Debye’s frequency, $\theta_D$ is Debye’s temperature [8], $\hbar = h/2\pi$ and $k_B$ are Planck’s and Boltzmann’s constants, respectively. When describing the plastic flow, a problem arises of matching the characteristic scales $\lambda$ and $\chi \ll \lambda$ and the velocities $V_{aw}$ and $V_t \gg V_{aw}$. It was shown earlier that quantities, $\lambda$, $\chi$, $V_{aw}$ and $V_t$, are related by the elastic–plastic strain invariant [5]:

$$\frac{\lambda V_{aw}}{\chi V_t} = \hat{Z} \approx \frac{1}{2}$$

It reflects the mutual causality of the elastic and plastic deformation processes in the medium in the course of plastic flow [5].

The major aim of this paper is the search for a correlation of the invariant $\hat{Z}$ and the plasticity parameter ($\lambda \cdot V_{aw}$), with the position of the metal in the periodic table of elements.

### 2. Materials and Methods

The studies of localized plastic flow were performed for nineteen metals from the 3rd, 4th, 5th, and 6th periods of the periodic table of elements. They are listed in Table 1. The numbers of conduction electrons $n$ per unit cell (the electron density) [9] are also given. The position of the elements in the periodic table is defined by the electron structure of the atoms. Thus, the number $N$ of the period gives the number of electron shells of the corresponding atoms, just as the group number $n$ for investigated metals, except transition metals Fe, Co, and Ni, coincides with electron density (see above).

### Table 1. The metals investigated and the elastic–plastic strain invariant.

| Periods | Lines | Metals | Groups of Periodical System of Elements | $\frac{\lambda V_{aw}}{\chi V_t} = \hat{Z}$ |
|---------|-------|--------|----------------------------------------|-------------------------------------------|
| 3       | III   | 12Mg   | 13Al                                   | 0.57 ± 0.63                               |
| 4       | IV    | 22Ti   | 23V                                   |                                             |
|         |       | 26Fe*  | 27Co                                   |                                             |
|         |       | 28Ni   |                                        |                                             |
| 5       | VI    | 40Zr   | 41Nb                                   | 0.48 ± 0.15                               |
|         | VII   | 50Sn   | 52Mo                                   |                                             |
| 6       | VIII  | 72Hf   | 73Ta                                   | 0.69 ± 0.45                               |
|         | IX    | 82Pb   |                                        |                                             |

$n$ [9] 1 2 3 4 5 6 8 9 10

*The alloys on the base both $\alpha$-Fe and $\gamma$-Fe were used in these experiments.*
Specimens with a 2 mm × 10 mm × 50 mm gage portion were subjected to tensile tests at a rate = 6.7 × 10⁻⁵ s⁻¹ and 300 K on an Instron-185 tensile-testing machine (Instron, London, UK, and stress σ-strain ε curves were recorded. The tension strength test on metals was according to ASTM E8/E8M.

The autowave characteristics of the localized plastic strain required for the analysis were obtained from patterns of localized plasticity recorded by the speckle photographic method of deformation field analysis during elongation of flat samples described in detail in [10].

The distribution of the local deformation components over the specimen surface was realized from localized plastic flow pictures, and their shape was dependent on the operating law of strain hardening [10]. These pictures are the projection of a wave deformation process on the specimen surface. The step-by-step detection of displacement fields r (x, y), when a sequence of two exposure speckle photographs, each of which corresponds to a total-strain increment, Δεtot ≈ 0.2%, is taken along a flow curve, allowed us to analyze the run-time of plastic flow. Speckle images were taken along axes x and y at a step of 0.5 mm. The local strain distributions thus obtained characterize the local strain increment when the total tensile strain increases by Δεtot (rather than the total strain from the beginning of loading). Therefore, the absence of strain in the next speckle photograph only indicates the absence of a plastic deformation increment in the region under study at the given deformation step. An important problem is the contribution of plastic deformation in its localization zones to the total strain increment per loading step between two adjacent speckle photographs. A simple estimation demonstrates that the entire plastic deformation of a specimen concentrates in exactly these zones at a given time.

The plastic deformation of a specimen during tension is localized in a few relatively thin layers, and total strain should be considered as the sum of the strain contributions in all zones (see example in Figure 1). The kinetic characteristics of the development of macroscopically localized plasticity (the wavelengths λ and velocities $V_{aw}$) were found from the dependences of the coordinates of the detected deformation zones on the deformation time [10]. Since the total strain during tension at a constant rate is proportional to time ($ε_{tot}$ ~ t), we can determine the position X of the deformation localization zone (or several zones) $ε_{xx}$ along the specimen length during deformation, using the slope of the X–t curve, and calculate the velocity of the localized plastic flow zone, $V_{aw} = dX/dt$. The values for interplanar spacing $χ$ and transverse elastic waves, with the velocity $V_t$, were taken from numerous handbooks (see, for example, [11]).

![Figure 1. Spatial distribution of local elongations $ε_{xx}$ over the test sample Zr.](image)

3. Results

The experimental data provides persuasive evidence of the existence of correlations between the plasticity phenomena in solids and the element’s position in the periodic table of elements.
Our analysis demonstrated that the plasticity parameter, \((\lambda \cdot V_{aw})\), oscillates in its average value at least within \(12 \leq Z \leq 82\) (where \(Z\) is the atomic number of the element). Similar oscillating behavior is typical for certain independently determined lattice characteristics, such as Debye’s temperature, binding energy, elastic modulus, electron work function, etc. In Figure 2, we compare the periodic variation of the plasticity parameter \((\lambda \cdot V_{aw})\) with the atomic number \(Z\) of the element, and the same for binding energy, \(E_b\), and Debye’s temperature, \(\theta_D\) [3]. Therefore, these observations show that the electron structure of an atom plays a significant part in metal plasticity.

![Figure 2](image_url)

**Figure 2.** The oscillations in plasticity parameter, \((\lambda \cdot V_{aw})\) (1, ■), binding energy, \(E_b\) (2, •), and Debye’s temperature, \(\theta_D\) (3, ▲), by the increase of atomic number \(Z\); the reference data were used for the values \(E_b\) and \(\theta_D\).

Experimental studies of localized plastic flow were carried out on various metals belonging to periods 4–6 of Mendeleev’s periodic table of elements. The quantities characterizing the process of localized plastic deformation—the length and velocity of propagation of the phase autowave—were measured using the speckle photography technique. Analysis of the data set obtained for the stages of linear strain hardening made it possible to establish that, as the element number increases within \(12 < Z < 82\), the dependence of the plasticity parameter \((\lambda \cdot V_{aw})\) on the atomic number of the element \(Z\) oscillates relative to the average value. It was found that these oscillations correlate with the regularities of behavior with increasing \(Z\) of a number of independently defined lattice characteristics, such as, Debye’s temperature, density, melting point, elastic moduli, ionization potential, and some others [1,8]. As an example, the correlation of the discussed dependences is illustrated by those shown in Figure 2, including, in-phase behavior of the plasticity parameter \((\lambda \cdot V_{aw})\) and reference data for Debye’s temperature and binding energy as functions of the atomic number of the studied elements. Debye’s temperature is directly expressed in terms of the speed of sound propagation and, therefore, in terms of the elastic characteristics of a rigid body. Consequently, the symbate oscillations of the dependences in Figure 2 confirm the relationship between the elastic and plastic properties of the deformable medium.

There are linear correlations between plasticity parameter \((\lambda \cdot V_{aw})\), on the one hand, and certain physical properties of the investigated metals, on the other. Typical examples of similar correlations are shown in Figure 3a–d. From this data, it follows that the discussed dependencies vary according to the period number of the \(N\) of the investigated metal. Moreover, these findings are interesting because they concern both electron (Figure 3a) and ionic (Figure 3b–d) subsystems of metals.
Figure 3. The correlations of plasticity parameter with electron work function (a); bulk modulus (b); atomic volume (c); binding energy (d). The notations are as follows: ■–elements of 3rd–period (Mg, Al), •–elements of 4th–period (Ti, V, α-Fe, γ-Fe, Co, Ni, Cu, Zn), ▲–elements of 5th–period (Zr, Nb, Mo, Cd, In, Sn), ▼–elements of 6th–period (Hf, Ta, Pb).

From the literature changes in the values of binding energy, bulk modulus of elasticity, and atomic volume are well known, with a continuous increase in the serial number Z [1,3]. Typically, many characteristics of metals are measured in their elastic state [12]. With the presented data on the characteristics of plasticity and with the knowledge of the methods of extracting the information contained in them, researchers can obtain a large array of information about the properties of the material under consideration. This prompted the collection of information and the systematization of data on linear correlations between the characteristics of plasticity and other properties of metals, such as: work function of an electron, binding energy, bulk modulus of elasticity, and atomic volume, which are shown in Figure 3. As can be seen, the plasticity parameter in each period decreases with an increase in the electron work function, binding energy, and bulk modulus of elasticity, and increases with an increase in the atomic volume.

The data in Table 1 show that the experimental values of the invariant \( \langle \hat{Z} \rangle \) for the 3rd–6th periods of the periodic table differ somewhat from each other. The significance of these differences between pairs was evaluated statistically using paired data using Student’s t-test with a 90% confidence level [13].

As these evaluations showed, the differences between \( \langle \hat{Z} \rangle_3, \langle \hat{Z} \rangle_4, \langle \hat{Z} \rangle_5 \) and \( \langle \hat{Z} \rangle_6 \) are insignificant.

Based in this, one can suggest that these values belong to one general population. Averaging over all nineteen metals yields, \( \langle \hat{Z} \rangle_M \approx 1/2 \) coincides with the value taken together in [5] for metals and nonmetallic materials. This means that invariant \( \hat{Z} \) (1) is independent of the number of the period in the periodic table.
Analysis of the behavior of the plasticity parameter within each period of the periodic table demonstrated that the value \((\lambda \cdot V_{aw})^{-1}\) is proportional to the number \(n\) of the conduction electrons per unit cell of the metal, as shown in Figure 4a. A relationship of this type was already described in [14], but it only became possible to highlight the separation over the periods of the periodic table of elements after investigation of a sufficient number of metals.

Figure 4. The dependence of the plasticity parameter on the numbers of conduction electrons \(n\) per unit cell for metals of 3rd–6th periods (a); the dependence of the coefficient \(D\) in Equation (3) and the value \(\langle \Lambda \rangle_N\) in Equation (13) on number of periods (b).

Within each investigated period, the linear dependence:

\[ (\lambda V_{aw})^{-1} \approx C + Dn \]  

was observed, where the empirical coefficients \(C\) and \(D\) differed for the elements of the 3rd–6th periods. The value of \(D\) in Figure 4a denotes the slope of straight lines for different periods. The maximum value corresponds to the 5th period, the minimum value corresponds to the 6th period. Their physical sense is not discussed here. Experimental data analysis showed that coefficient \(D\) in Equation (2) depended on the period number, \(N\), as:

\[ D \approx D_0 \exp(-q/N) \]  

In other words, \(\ln D \sim N^{-1}\). Here, the number \(N\) takes the values 3, 4, 5, and 6, while \(D_0\) and \(q\) are constants. Equation (3) is illustrated in Figure 4b.

The explanation of the results above is focused on comparison of the invariant values for different periods and elucidation of the nature of the dependence of the autowave plasticity parameter \((\lambda \cdot V_{aw})\) on the electron density \(n\) for the metals, i.e., on the position of these elements in the periodic table of elements.

4. Discussion

It follows from Figure 4a and Equation (2) that \((\lambda \cdot V_{aw})^{-1} \sim n\) for metals of the 3rd–6th periods. The physical meaning of this proportionality results from the fact that one can easily go from the plasticity parameter \((\lambda \cdot V_{aw})^{-1}\) to de Broglie’s formula [12] for the effective mass:

\[ m_{ef} = \frac{h}{\lambda V_{aw}} \]  

Then, it follows from Figure 4a, that \(m_{ef} \sim n\). This fact was found earlier [14,15], where the effective mass was related to a quasi-particle associated with the localized plastic flow autowave and named autolocalizon.

The average effective masses calculated from Equation (4) yield \(\langle m_{ef} \rangle = 1.8 \pm 0.3 \approx 2\) a.m.u. (see Table 2). The differences among the average values \(\langle m_{ef} \rangle\) for 3rd–6th periods turn out to be statistically insignificant [13]. Statistical analysis using the procedure
described in [13] has shown that the distribution of the \( m_{\text{ef}} \) values about the average value is normal.

Table 2. The metals investigated and the elastic–plastic strain invariant.

| Period Number, \( i \) | 3 | 4 | 5 | 6 |
|-------------------------|---|---|---|---|
| Metal                   |  |  |  |  |
| Mg                      | 4.0 | 0.5 | 1.1 | 1.4 | 1.8 | 1.8 | 1.3 | 1.9 | 1.8 | 1.1 | 2.0 | 2.3 | 0.3 | 4.2 | 1.6 | 1.3 | 4.0 | 0.6 | 1.3 |
| \( \langle m_{\text{ef}} \rangle \), a.m.u. | 2.25 ± 1.7 | 1.52 ± 0.12 | 1.95 ± 0.52 | 1.97 ± 1.1 |
| \( \theta_D \), K [5] | 330 | 390 | 380 | 390 | 373 | 373 | 386 | 310 | 237 | 250 | 260 | 260 | 377 | 120 | 129 | 254 | 213 | 225 | 87 |
| \( \Lambda \times 10^5 \text{ m}^2/\text{s} \) | 2.8 | 4.4 | 5.9 | 5.9 | 4.4 | 4.4 | 4.4 | 3.7 | 9.2 | 9.8 | 6.4 | 6.4 | 11.8 | 12.9 | 11.8 | 10.7 | 4.0 |
| \( \langle \Lambda \rangle \times 10^5 \text{ m}^2/\text{s} \) | 3.6 ± 0.8 | 4.3 ± 0.5 | 7.2 ± 0.9 | 8.8 ± 2.7 |

Atomic mass unit (a.m.u.) is equal to \( 1.66 \times 10^{-27} \text{ kg} \).

To explain the origin of the effective mass \( m_{\text{ef}} \), one must recall that plastic flow is the result of dislocation jumps between local barriers [16]. The waiting time of the jump, \( \Theta \), is thermally activated. The time of the jump is \( \tau \ll \Theta \). It is essential that dislocations are immobile during time \( \Theta \), and the plastic deformation at that time does not increase. It increases by dislocation jumps during time \( \tau \), and their dynamics are controlled by the viscosity of phonon and electron gases [17,18].

To discuss the nature of the effective mass \( m_{\text{ef}} \), two regimes of dislocation motion should be considered. Let, \( V_{\text{disl}} = \text{const} \) and, \( V_{\text{disl}} \neq 0 \), the viscous drag force per unit length of the dislocation line will be:

\[
F_{\text{vis}} \approx BV_{\text{disl}} \sim V_{\text{disl}}
\]

where \( B \approx (10^{-5} - 10^{-4}) \text{ Pa} \cdot \text{s} [17] \) is the viscous drag coefficient for dislocation. This coefficient for metallic crystals is determined by the properties of the electron and phonon gases [17,18].

In a more realistic case, when \( V_{\text{disl}} \neq \text{const} \) and \( V_{\text{disl}} \neq 0 \), the inertial term \( F_{\text{in}} \) arises being proportional to the dislocation acceleration (\( V_{\text{disl}} \neq 0 \)). In this case, the total drag force per unit length of the dislocation line would be written [19]:

\[
F_{\Sigma} = F_{\text{vis}} + F_{\text{in}} \approx BV_{\text{disl}} + \frac{B}{v} \cdot V_{\text{disl}} = B \left( V_{\text{disl}} + \frac{V_{\text{disl}}}{v} \right)
\]

In metals, the contributions of the phonon and electron gases into the viscous dislocation drag coefficient are additive [17], i.e., \( B = B_{\text{ph}} + B_e \). Thus, it follows from Equation (6) that:

\[
F_{\Sigma} \approx B_{\text{ph}} V_{\text{disl}} + B_e V_{\text{disl}} + \frac{B_{\text{ph}}}{v} V_{\text{disl}} + \frac{B_e}{v} V_{\text{disl}}
\]

Here, \( v \) is the acting frequency of deformation. In this case, \( B/v \) and can be interpreted as the attached mass per unit dislocation length. This conclusion agrees with Eshelby’s opinion [20] that the dislocation motion is similar to the motion of the Newtonian particles. In this case, the third and fourth terms on the right-hand side of Equation (7) define the attached mass, that is:

\[
F_{\text{in}} \approx \frac{B_{\text{ph}}}{v} V_{\text{disl}} + \frac{B_e}{v} V_{\text{disl}} \sim m_{\text{ef}} \sim n
\]

Thus, the value, \( m_{\text{ef}} \), can be regarded as the attached mass associated with the accelerated motion of plasticity carriers (dislocations) in the viscous medium [16,17].

The term \( B_e/v \) has special interest in Equation (8). According to the data presented in [17], the viscosity of the electron gas is proportional to electron density, that is, \( B_e \sim n \). From here, the explanation follows of the proportionality, \((\lambda \cdot V_{\text{aw}})^{-1} \sim m_{\text{ef}} \sim n\) where it
describes the influence of the electron gas density to the dislocation motion drag. As for the role of the attached mass associated with the phonon gas viscosity, $B_{ph}/\nu$, it weakly depends on the properties of metals at temperatures, $T > \theta_D$ [8].

The correlations in Figure 4a are manifested through the change in the characteristics of localized plasticity autowave motion at the linear work hardening stage depending on electron density. They are explained by the contribution of the electron gas to dislocation drag. The obtained data indicate directly that the nature of the electron gas contribution to dislocation drag is more complex in character than the traditional theories of this effect originally envisaged.

It follows from the data obtained that the relation:

$$ (\lambda \cdot V_{aw}) \sim \exp\left(\frac{\chi^*}{\chi}\right) $$

holds true for the elements of the 3rd–6th periods, as shown in Figure 5. An especially interesting trait is found for the elements of the 4th and 5th periods, where eight and six metals were investigated, respectively. It is of importance that the constant $\chi^*$ is close to the interplanar distance corresponding to the maximal intensities of X-ray reflection for potassium and rubidium, from which the 4th and 5th periods begin. It was established, for the 4th period, $0.37 = \chi^*_4 \approx \chi_K = 0.375 \text{ nm}$, and for the 5th period, $0.45 = \chi^*_5 \approx \chi_{Rb} = 0.433 \text{ nm}$. This consideration creates a possibility of predicting the character of plastic flow patterns in metals, using their lattice characteristics only.

![Figure 5](image-url)

**Figure 5.** The dependence of the plasticity parameter on interplanar distance for metals of 3rd–6th periods.

The experiments showed that the plasticity parameter, $(\lambda \cdot V_{aw})$ increases with Debye's temperature, $\theta_D$, as shown in Figure 6a. It is convenient, here, to introduce a characteristic temperature, $T^* = E_b/k_B$, and to use then the dimensionless temperature, $\theta_D/T^*$. Then, the dependence of, $(\lambda \cdot V_{aw})$ on $\theta_D/T^*$ is:

$$ (\lambda V_{aw}) = \Lambda \frac{\theta_D}{T^*} $$

where coefficient, $\Lambda = (4.4 \pm 1.3) \cdot 10^{-5} \text{ m}^2/\text{s}$, and the correlation coefficient between values, $(\lambda \cdot V_{aw})$ and $\theta_D/T^*$ is close to 0.8.
To understand the physical meaning of Equation (10), we use the following consideration. There are a number of consequences from invariant (1) describing the various features of plastic flow [5]. One can suppose that Equation (10) is one of these consequences. As a result, Equation (1) can be rewritten in the form:

$$\lambda V_{aw} = \hat{Z} \chi V_t$$

(11)

Using the above introduced relations, $V_t/2\chi = \omega_D$ and $k_B\theta_D \approx \hbar\omega_D$, we obtain:

$$\langle \lambda V_{aw} \rangle \approx (2\hat{Z} \chi^2 k_B T^*/\hbar) \cdot \frac{\theta_D}{T^*}$$

(12)

that is, Equation (12) follows from Equation (1). In this case, we have:

$$\Lambda_{calc} = (2\hat{Z} \chi^2 k_B T^*/\hbar) = \left(2\hat{Z} \chi^2 \frac{E_b}{K}\right) \approx \chi^2 \frac{E_b}{K}$$

(13)

Now, one can calculate the quantities of $\Lambda_{calc}$ using the published values $\chi$ and $E_b$ for all the metals. The results of calculations are shown in Table 2. The average coefficient is, $\langle \Lambda_{calc} \rangle = (5.8 \pm 1.5) \cdot 10^{-5}$ m$^2$/s; the difference between this quantity and the coefficient in Equation (10) is not statistically significant, according to the statistical procedure [13].

One can present the dependence $\langle \lambda V_{aw} \rangle \sim \theta_D/T^*$ in another manner. In reality, the averaging of values $\Lambda$ for metals of one period, as it is shown in Table 2, allows one to find the quantities $\langle \Lambda \rangle_N$ for every period, as shown in Figure 4b, $\langle \Lambda \rangle_N \sim N$ (or $\langle \Lambda \rangle^{-1}_N \sim N^{-1}$). The values found are significantly different. This allows one to break the dependence, $\langle \lambda V_{aw} \rangle \sim \frac{\theta_D}{T^*}$ into four parts by the period number, as shown in Figure 6b.

The above considerations point to the existence of a relationship between the plasticity parameter ($\lambda \cdot V_{aw}$) and the lattice properties. Moreover, the appearance of Planck’s constant, $\hbar$, in Equation (13), together with typical mechanical characteristics, confirms the appropriateness of the use of quantum mechanical ideas in plasticity physics, as was proposed by us in [15,21].

5. Conclusions

The present study elucidates several features of localized plasticity of metals related to their position in the periodic table of elements. It is shown that the correlation exists between plasticity characteristics and the electron structure of metal atoms—the number of electrons per unit cell $n$. The mechanism based on the existence of a relationship between the moving dislocations and the electron gas is indirectly confirmed by investigations performed in [22] that relate the electric potential on the surface of a deforming metal sample with entrainment of conduction electrons by moving dislocations during jump-like plastic deformation.
Thus, the plasticity of metals is largely determined by their position in the periodic table of elements. Results of quantitative experimental research of the characteristics of the localized plastic flow development for nineteen metals belonging to the 3rd–6th periods of the periodic table of elements have shown the following:

1. The value of the elastic–plastic strain invariant, \( \hat{Z} = \lambda V_{aw}/\chi V_t \), is independent of the position of the element in the periodic table of elements and can be considered the universal characteristic of plastic deformation;

2. The plasticity parameters, \((\lambda \cdot V_{aw})\), correlate with the period and group number of the deforming metal in the periodic table of elements, which is due to the dislocation drag by viscous electron gas;

3. The data obtained can serve as a possible basis for prediction of plastic properties of metals and alloys. However, this will require further research.

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