Abstract

LHC collisions can act as a source of photons in the initial state. This mechanism plays an important role in the production of particles with electroweak couplings, and a precise account of photon-initiated (PI) production at the LHC is a key ingredient in the LHC precision physics programme. I will discuss the possibility of modelling PI processes directly via the structure function approach. This can provide percent level precision in the production cross sections, and is therefore well positioned to account for LHC precision requirements. This formalism in addition allows one to make use of another useful feature of photons, namely that they are colour-singlet and can often be emitted elastically (or quasi-elastically) from the proton. I will discuss recent work on applications of the structure function approach to precision calculations of PI production in the inclusive mode, and to ‘exclusive’ processes with rapidity gaps, which can provide a unique probe of the Standard Model and physics beyond it.

1 Introduction

A major aim of the LHC, and the HL–LHC upgrade that will follow, is to precisely test the Standard Model (SM) predictions for as wide a range of collider processes as possible. A particularly important element of this involves events with leptons in the final state, which play a key role in determinations of the weak mixing angle, $\sin^2 \theta_W$, the $W$ boson mass, $M_W$, and constraints on the proton PDFs. A key ingredient in this is the availability of high precision theoretical predictions for the SM processes, an important element of which is the contribution from the photon–initiated (PI) channel.

A further feature of this channel in proton–proton collisions is that the colour singlet photon exchange naturally leads to exclusive events, where the photons are emitted elastically from the protons. This is particularly relevant in the context of the dedicated forward proton detectors at the LHC, namely AFP and CT–PPS, which have been installed in association
with both ATLAS and CMS, respectively [1]. More generally, even if the initial–state photon is emitted inelastically, there is no colour flow as a result, and there is still a possibility for semi–exclusive events with rapidity gaps in the final–state between the proton dissociation system(s) and the centrally produced object. Indeed, a range of data have been collected using this technique at the LHC [2].

Here, we present the application of the so–called structure function (SF) method to the calculation of both the PI component of inclusive lepton production, at high precision, and PI production in the exclusive mode.

2 The Structure Function Approach and inclusive photon–initiated production

The SF framework is a rather useful method [3,4] for calculating the PI lepton pair production cross section directly in terms of the proton structure functions. For processes such as (off Z–peak) lepton pair production this provides percent precision in the predicted cross sections, with no accompanying factorization scale variation uncertainty, as is present in the calculation within collinear factorization.

![Graph](https://example.com/graph.png)

Figure 1: (Left) Ratio of the PI cross sections for lepton pair production to the NLO QCD Drell–Yan cross section at the 13 TeV LHC. The LO collinear predictions (including scale variation uncertainties) and the structure function result are shown, in the latter case for both the pure $\gamma\gamma$ initiated and the total. (Right) Percentage contribution from PI production to the lepton pair $p_{\perp}$ distribution, within the ATLAS [5]–off–peak event selection, at 8 TeV. The QCD predictions correspond to NNLO + NNLL QCD theory [6]. The total (pure $\gamma\gamma$) contributions are shown by the solid (dashed) lines.

In the SF approach, the PI cross section is given by

$$
\sigma_{pp} = \frac{1}{2s} \int \frac{d^3 p_1 d^3 p_2 d\Gamma}{E_1 E_2} \alpha(Q_1^2) \alpha(Q_2^2) \rho_{\perp}^{\mu \nu} \rho_{\perp}^{\nu \mu} M_{\mu \nu}^* M_{\mu \nu} \delta^{(4)}(q_1 + q_2 - k). \quad (1)
$$

Here the outgoing hadronic systems have momenta $p_{1,2}$ and the photons have momenta $q_{1,2}$, with $q_{1,2}^2 = -Q_{1,2}^2$. We consider the production of a system of 4–momentum $k = q_1 + q_2 = \sum_{j=1}^{N} k_j$ of $N$ particles, where $d\Gamma = \prod_{j=1}^{N} d^3 k_j / 2E_j (2\pi)^3$ is the phase space volume. $M_{\mu \nu}$ corresponds to the $\gamma\gamma \rightarrow X(k)$ production amplitude, with arbitrary photon virtualities. $\rho$ is the density matrix of the virtual photon, which is given in terms of the well known proton structure functions, see [3,4] for an explicit expression and [4] for the extension to include initial–state Z bosons.
A representative selection of results are shown in Fig. 1. In the left plot we show the lepton pair invariant mass distribution, plotting the ratio of the PI contribution to the NLO QCD Drell–Yan cross section at the 13 TeV LHC. For this choice of cuts, the PI component is at the ∼4% level, and hence is small but certainly not negligible. We note that the solid curve includes the uncertainty due to the experimental determination of the structure functions, but this is so small as to not be visible on the plot. The ‘total’ contribution includes initial–state Z boson, and mixed γ/Z + q contributions, but these are found to give a negligible contribution. The LO collinear result is also shown for comparison. This is seen to lie above the SF results, though consistent within the large scale variation uncertainties; clearly, one should work at least at NLO when applying the collinear approach. However, for the present observable we can see that the SF approach provides percent level precision already.

Above the Z peak (not shown here), the PI contribution is as large as ∼10%, and can again be predicted with high precision by the SF approach. As discussed in further detail in [4], these results imply that the PI contribution to the dilepton cosθ∗ distribution, which is used for determinations of sin²θW as well as PDF constraints, can also be highly relevant. Detailed comparisons are presented in [4] and this is indeed found to be the case, with the SF approach providing high precision predictions for the PI contribution.

As the SF formulation of Eq. 1 is provided differentially with respect to the photon virtualities, Q², we can also readily provide predictions with respect to the dilepton transverse momentum, p⊥. In Fig. 1 (right) we show the ratio of the PI contribution to NNLO+N3LL resummed QCD predictions produced with NNLOjet+RadISH [6]. The solid curve includes mixed γ + q diagrams, which will be sensitive to resummation effects in the low p⊥ region, not included here, is only shown for rough guidance in this region. Focussing on the pure γγ component, i.e. the dashed lines, one can see a significant enhancement observed in the pure γγ contribution in the lower 0 < p⊥ < 2 GeV region. This is explained in part by the Sudakov suppression in the QCD contribution in this region, which is absent in the γγ channel. However, another key factor in this is that the γγ cross section is particularly peaked in this region, due to the significant contribution from elastic photon emission. This elastic component, or indeed the low Q² resonant and non–resonant components, are not modelled differentially in a pure collinear calculation, and hence the SF calculation is particularly well suited to deal with this very low p⊥ region. As explored in [4], this could have implications for experimental determinations of MWW, through the tuning that is done to the low p⊥ region of dilepton production.

Finally, we note that the benefit of applying the SF approach directly, while transparent for process where the final state of interest (l⁺l⁻, W⁺W⁻...) is directly produced by the γγ initial state, is less clear in the mixed γ + q case. Here, one must deal with the collinear enhancement of the γ → q̅q splitting, and at this level of precision include QED DGLAP evolution of the quark/antiquark PDFs, which certainly requires one introduce a photon PDF within the LUXqed approach. Further discussion can be found in [4].

3 Modelling (semi)–exclusive photon–initiated production

This theoretical treatment of exclusive and semi–exclusive events is rather distinct from the standard inclusive case. The reasons for this are twofold: first, if events are selected with a rapidity veto then the case where decay products from the proton dissociation system enter the veto region must be excluded, and second, there may be additional inelastic proton–proton QCD interactions (in other words, underlying event activity) that fill the gap region. The latter effect must be accounted for via the so–called ‘survival factor’ probability of no additional proton–proton interactions [7], while the former requires a fully differential treatment of the
PI process, including a MC implementation such that the showering and hadronisation of the dissociation system may be accounted for.

In [2], we presented such a MC implementation, SuperChic 4, for the case of lepton pair production. This makes use of the SF approach, to provide a high precision prediction for the underlying PI process that is fully differential in the kinematics of the final–state protons and/or dissociation systems. This can then be interfaced to a general purpose MC for further showering/hadronization; we make use of Pythia 8.2 [8]. We in addition account for the survival factor, in a manner that takes full account of the dependence of this quantity on the event kinematics and the specific channel (elastic or inelastic). SuperChic 4 is the first generator of its kind to take account of all of these features, which are essential when providing results for semi–exclusive PI production.

In Fig. 2 (left) we show the predicted survival factor as a function of the dimuon invariant mass, $M_{ll}$, of the dilepton system. (Right) Comparison of SuperChic 4 + Pythia 8.2 predictions for the dilepton acoplanarity distribution compared to the ATLAS data [9] at $\sqrt{s} = 7$ TeV, within the corresponding experimental fiducial region, and with a rapidity veto applied on tracks in the central region. Results without the soft survival factor included are shown in addition.

Figure 2: (Left) Soft survival factor for lepton pair production as a function of the invariant mass, $M_{ll}$, of the dilepton system. (Right) Comparison of SuperChic 4 + Pythia 8.2 predictions for the dilepton acoplanarity distribution compared to the ATLAS data [9] at $\sqrt{s} = 7$ TeV, within the corresponding experimental fiducial region, and with a rapidity veto applied on tracks in the central region. Results without the soft survival factor included are shown in addition.
4 Conclusion

In summary, PI production is a rather unique channel at the LHC that plays a key role in both inclusive and exclusive particle production. We have presented state-of-the-art results for dilepton production in both of these channels, including MC implementations; SFGen [4] and SuperChic 4 [2] for inclusive and exclusive production, respectively.

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**References**

[1] C. Royon and N. Cartiglia, *The AFP and CT-PPS projects*, Int. J. Mod. Phys. A 29, 1446017 (2014), doi:10.1142/S0217751X14460178.

[2] L. A. Harland-Lang, M. Tasevsky, V. A. Khoze and M. G. Ryskin, *A new approach to modelling elastic and inelastic photon-initiated production at the LHC: SuperChic 4*, Eur. Phys. J. C 80, 925 (2020), doi:10.1140/epjc/s10052-020-08455-0.

[3] L. A. Harland-Lang, *The proton in high definition: revisiting photon-initiated production in high energy collisions*, J. High Energy Phys. 03, 128 (2020), doi:10.1007/JHEP03(2020)128.

[4] L. A. Harland-Lang, *Physics with leptons and photons at the LHC*, Phys. Rev. D 104, 073002 (2021), doi:10.1103/PhysRevD.104.073002.

[5] G. Aad et al., *Measurement of the transverse momentum and \( \phi_\eta^* \) distributions of Drell–Yan lepton pairs in proton–proton collisions at \( \sqrt{s} = 8 \text{ TeV} \) with the ATLAS detector*, Eur. Phys. J. C 76, 291 (2016), doi:10.1140/epjc/s10052-016-4070-4.

[6] W. Bizoń et al., *Fiducial distributions in Higgs and Drell-Yan production at \( N^3 LL + NNLO \)*, J. High Energy Phys. 12, 132 (2018), doi:10.1007/JHEP12(2018)132.

[7] L. A. Harland-Lang, V. A. Khoze, M. G. Ryskin and W. J. Stirling, *Central exclusive production within the Durham model: A review*, Int. J. Mod. Phys. A 29, 1430031 (2014), doi:10.1142/S0217751X14300312.

[8] T. Sjöstrand et al., *An introduction to PYTHIA 8.2*, Comput. Phys. Commun. 191, 159 (2015), doi:10.1016/j.cpc.2015.01.024.

[9] G. Aad et al., *Measurement of exclusive \( \gamma\gamma \rightarrow \ell^+\ell^- \) production in proton–proton collisions at \( \sqrt{s} = 7 \text{ TeV} \) with the ATLAS detector*, Phys. Lett. B 749, 242 (2015), doi:10.1016/j.physletb.2015.07.069.