Abstract: A new type of collar, the hooked-collar, was studied through experiments and numerical methods. Tests were conducted using a hooked collar of a width of 1.25b and a height of 0.25b, where b is the bridge-pier width. The hooked-collar efficiency was evaluated by testing different hooked-collar placements within the bridge-pier, which were compared to the bridge-pier without any collar. A double hooked-collar configuration, one placed at the bed level and the other buried 0.25b, was the most efficient at reducing the scour hole. In other cases, a hooked-collar positioned 0.25b above the bed slightly reduced the scour hole and had similar scour patterns when compared to the pier without the hooked-collar. The flow fields along the vertical symmetrical plane in the experiments are also presented. Laboratory experiments and numerical tests show that maximal downflow is highly reduced along with a corresponding decrease in horseshoe vortex strength for the experiments with the hooked-collar, compared to cases without the hooked-collar. The flow fields reveal that the maximum turbulent kinetic energy decreases with the installation of the hooked-collar.

Keywords: bridge; collar; hooked-collar; pier; scour

1. Introduction

Local scour around a hydraulic structure such as a bridge pier or abutment is caused by the enhanced transport capacity of sediment around a structure and by the formation of vortices. Excessive local scouring compromises the stability of these structures and has been attributed to be the main cause of bridge pier failure [1,2]; hence, reducing the maximum local scour depth at bridge piers has been a topic of safe design. The flow field at a pier is coupled with a complex horseshoe vortex system initiated from the downflow upstream of the pier, which is thought to be the major impelling process behind the growth of the scour depth, and wake vortices downstream of the pier [3,4]. These vortices create scour holes around the pier when the shear stress on the stream bed becomes greater than the critical shear stress. Because of the nature of the flow field, two methods are commonly used to reduce scour depth. The first consists of increasing stream bed resistance to withstand erosion. This is done by placing armorig devices at the bed level, such as riprap (could be a non-movable, coarse and non-cohesive material) and bed sills [5–7], which provides a physical barrier to resist the erosive power of the flow. Four mechanisms are included in riprap failure: shear failure due to stones not being able to withstand the hydrodynamic forces by the flow; winnowing failure due to scouring of the underlying soils; edge failure by erosion at the borderline of the riprap; and live bed failure [7,8].
Most previous studies have focused on designing the size, layer thickness and extent of the riprap layer [7–9]. Critical velocity often dictates the size. In a combined setup of riprap and collar by Mashahir et al. [10], scour volumes were reduced by up to 57%. Besides, Hamidifar et al. [6] applied bed sills to reduce scour depth, and in their investigations, they reduced upstream and downstream scour by 23% and 47%, respectively. Attaching a collar to the pier reduces the downflow and, subsequently, the formation of the horseshoe vortex. The collar changes the flow pattern around the pier by deflecting the downflow and decreasing the horseshoe vortex. Several research works have reported the effectiveness of collars in reducing the local scour depth around piers [11–16]. Singh et al. [14] concluded that the efficacy of a collar in preventing scour is a function of its width and its elevation relative to the bed surface. They found that a collar width of 2b wide placed at −0.1b, where b is the pier width, resulted in a maximum reduction in scour depth for circular piers. Zarrati et al. [15] showed that a collar three-times the pier diameter is effective at reducing scour depth for rectangular piers. Previous studies have shown that collar performance is dependent on its size and its location with respect to the stream bed. In evaluating trapezoidal collars, Khosravinia et al. [17] demonstrated better collar performance with increasing width. Scour depth decreased by up to 37%. However, installing a large collar may be a challenge in practical engineering. Earlier investigations by [10,18] found collars with widths greater than 3b impractical.

Considering the economics and ease of construction, reducing collar width is essential. This study proposes a new type of collar, the hooked-collar, with reduced width when compared to previous works [13,15]. Figure 1 shows schematic flow features around piers fitted with a collar and a hooked-collar. The collar reduces the strength of the horseshoe vortex by deflecting the downflow further from the pier. The hooked-collar attaches to a thin ring outside the collar, deflecting the downflow in an upward direction, resulting in a weak downflow by which the pier may benefit. The study further provides guidance to the choice of collar location with respect to the pier and channel bed following earlier investigations by [18].

Finally, to better understand the hydraulics and the effects of using the proposed hooked-collar, numerical models are essential in addition to physical tests or experiments. Henceforth, the study further validated laboratory experiments using a 3D numerical model, FLOW-3D.

![Figure 1](image1.png)

**Figure 1.** Flow features around piers: (a) pier fitted with a collar; and (b) pier fitted with a hooked-collar.

### 2. Experimental Setup and Procedure

Experiments were carried out in an 8 m-long, 0.3 m-wide and 0.6 m-deep glass-sided re-circulating flume (Figure 2). A head tank located at the upstream of the main channel acted as a reservoir for
controlling flow discharge into the main channel. An electromagnetic valve controlled the flow discharge in the flume such that it was fixed at 0.011 m$^3$ s$^{-1}$. At the entrance of the main channel, a trumpet-shaped inlet and a honeycomb smoothly guided the inflow to guarantee uniform flow distribution, and at the outlet, a tailwater gate regulated and maintained flow depth.

![Diagram](image_url)

**Figure 2.** The flume system used for the experiments: (a) side view and (b) schematic diagram of the bridge pier and coordinate system. 1. Head tank. 2. Flow straightener. 3. Control panel. 4. Acoustic Doppler Velocimeter (ADV). 5. Pier. 6. Sediment bed. 7. Main channel. 8. Tailwater gate. 9. Re-circulating tank. 10. Pump. 11. Re-circulating pipe.

Figure 2 shows a definition sketch of the working section. A circular cylinder of diameter $b = 4$ cm was embedded at 5 m downstream of the flow straightener (see Figure 2a). Bridge piers were simulated from Polyvinyl Chloride (PVC), while hooked collars of a 3 mm thickness were made from Perspex. Observations made by Alabi [11] that collars whose thicknesses were less than 5 mm had no adverse impacts on scour depth development guided the selection of the hooked collar thickness. The flume channel was covered by a 10-cm thin layer of well-sorted sand having a median grain size of 0.69 mm with geometric standard deviation $\sigma_g = (d_{84}/d_{16})^{0.5} < 1.20$. Bridge pier diameter ($b$) was selected to negate the effect of lateral walls on the scour pattern around the circular cylinder [19], yielding a ratio of $H = 5b$, where $H$ is the flow depth, a ratio not deviating much in practice. Additionally, following the work of [2], we eliminated the effects of grain size on scour depth by the following condition: $b/d_{50} > 25$. A hooked collar with a width ($w$) of 1.25$b$ and a height ($h$) of 0.25$b$ was used in the experiments. Experiments were run under a clear water scour regime for 0.011 m$^3$ s$^{-1}$ of discharge with a 0.20-m flow depth; depth was selected such that it was greater than 3.5 times the diameter of the pier, thus eliminating its effect on the scour rate [19]. To avoid undesirable scour of the bed before the tests, the flume was initially filled with water until the required flow depth was reached. Discharge was gradually increased to the required depth. To enforce the clear water condition, the average approaching flow was set to 0.9 of the critical velocity, which was calculated from the Shields’ diagram. Scour depths were measured by a point gauge, to an accuracy of ±0.5 mm. An equilibrium state of scour was attained when the scour depth did not change by more than 1 mm over a period of 6 h. Two series of experiments were conducted: one with the collar and the other without. Hooked-collars were placed at two bed levels, 0.25$b$ above the bed and at the bed level. Earlier experiments by [18]...
guided the placement of the hooked-collars at the bridge piers. Experimental runs lasted more than 60 h when an equilibrium state of scour was reached. At this state, velocity samples were taken and scour profiles recorded. A down-looking Acoustic Doppler Velocimeter (ADV), developed by SonTek, was used for velocity measurements. Measurements were conducted along the vertical symmetrical plane. At each measurement line, velocities were taken over the entire flow depth at heights separated by 0.5∼1.0 cm. Flow velocity data at each position were recorded with a frequency of 25 Hz for 5 min. These data were used to compute statistical properties, including time averaged velocities, Reynolds stresses and turbulent kinetic energy (k).

3. Numerical Simulations

3.1. Model Setup

The increase in computational power has soared the application of numerical methods to investigate scour in hydraulic structures. Burkow and Griebel [20] applied NaSt3D (Institute for Numerical Simulation, Bonn, Germany) to simulate sediment transport and scouring at a rectangular obstacle. A Computational Fluid Dynamics (CFD) model was modified by Xiong et al. [21] based on Eulerian two-phase flow theory for bridge scour simulations. Török et al. [22] applied the 3D Reynolds averaged Navier Stokes Equation (RANS) with the κ-ε model to account for turbulence. In modeling local scour, Cheng et al. [23] developed an approximate methodology to account for the influence of coherent structures on pier scour RANS simulations. Besides the RANS model, more advanced models, demanding even much higher computational resources, have been used. Kirkil et al. [24] applied a Detached Eddy Simulation (DES) to study turbulence at a circular pier having a scour hole.

In this study, we use FLOW-3D, a state of the art commercial software developed by Flow Science (Santa Fe, NM, USA), to solve the RANS equations with the Renormalized Group (RNG) turbulent closure, on a structured mesh. Since the grain size used in this study was between 200 and 2000 µm [22], bed load sediment transport was computed by the van Rijn equation. The critical Shields number was computed from the Shields curve using the Soulsby-Whitehouse equation [25].

FLOW-3D contains a very simple, faster, yet powerful meshing capability through the Fractional Area/Volume Obstacle Representation (FAVOR). This method offers an accurate way of representing complex features (Figure 3) in the computational domain without the need of a fitted grid. It applies a collection of distinct algorithms to enhance numerical stability, compute interfacial areas, advection and stress along solid boundaries [25]. The computational mesh applied in this study contained 1.3 million cells in 3 mesh blocks (outer, intermediate and inner) having uniform edge lengths of 0.01, 0.008 and 0.005 m, respectively. The outer block was located at cells farther from the pier, while the dense inner block had piers and hooked collars installed (inner block shown in Figure 3). A compromise had to be made between a very fine mesh and computational costs. A finer mesh could accurately capture the hooked collar; moreover, the simulation time would have significantly increased; hence, we opted not to use it. Additionally, Bayon et al. [26] when evaluating the performance of FLOW-3D and Open-FOAM observed that FLOW-3D appeared less dependent on mesh size so long as the geometry was well favorized. Maximum aspect and adjacent cell ratios determined the cell size distribution within the blocks. These were respectively 1.02 and 1.03, which were well within the recommended limits of 3 and 1.2 [25].

Dimensions of the computational domain, pier and parameters of the simulations corresponded to the experimental setup as outlined in Section 2. At the inlet boundary, flow was fixed at a constant discharge of 0.011 m³ s⁻¹ following the laboratory setup, while at the outlet, a pressure boundary condition was fixed with a fluid elevation of 0.2 m. To ensure correct discharge at the inlet boundary, the computational domain was extended by −0.5 m in the upstream direction. No slip boundary conditions were specified at the bottom and in lateral walls corresponding to sidewalls, which assigned zero tangential velocity at the solid surfaces. The free surface, z max, was treated as stagnation pressure and zero fraction fluid. The maximum turbulent mixing length and time step were dynamically
computed by the FLOW-3D code. To initialize the FLOW-3D model, a constant water depth of 0.3 m was set in the computational domain, which allowed stability and faster convergence times.

Figure 3. An example of (a) a bridge pier and the hooked-collar installation, as well as the inner mesh block and (b) favorized image showing the hooked-collar geometry.

3.2. Model Validation

The laboratory experiment in Section 2 was used to validate the model. Figure 4 shows the comparison of maximum time-dependent scour depth observed in the laboratory and that of simulation. Numerical results agree well with experimental data, despite FLOW-3D slightly overestimating the scour depth beyond the 25 s of simulation for the no collar and the hooked-collar placed at 0.25b above the bed. Moreover, it underestimated the maximum time-dependent scour depth of the hooked-collar placed at the bed level (Figure 4).

Figure 4. Scour development for the different hooked-collar configurations.

4. Experimental Results

4.1. Hooked-Collar on Scour

Figure 4 depicts observed scour patterns around a pier without a hooked-collar and piers fitted with hooked-collars at different locations. The scour process of the single pier was consistent with those reported by several studies [14,27–29]. Initially, the downflow dug a hole directly in front of the pier (Supplementary Information, Figure S1). A horseshoe vortex removed the sediment from
around the base of the pier, resulting in the development of a scour hole. As the scour depth increased, the strength of the horseshoe vortex reduced, leading to a lower sediment transport rate from the base region. An equilibrium state was eventually established when the transport rate from the base region is equal to the transport rate into the region. In addition to scour around the pier, sediment deposition occurred immediately downstream of the pier. The scour processes of the pier with a hooked-collar differed from that without a hooked-collar. For the pier with a hooked-collar placed at 0.25b above the bed, two grooves first developed downstream of the pier and moved upstream along the rim of the pier (Supplementary Information, Figure S2). The scour hole later formed along the upstream face of the pier. As these depressions joined each other at the downstream edge of the pier, the scour process returned to the action of the horseshoe vortex, similar to the case of a single pier. For the piers with a hooked-collar placed at the bed level (Supplementary Information, Figure S3), the scour hole was first observed in a region ±90 of the pier. Two grooves gradually developed at the downstream rim of the collar and extended downstream. No scour was observed at the immediate upstream of the pier.

The pier without a hooked-collar resulted in maximum scour depth (Figure 5). The hooked-collar positioned 0.25b above the bed reduced the scour hole by 24%, compared with the pier without a hooked-collar. Installing the hooked-collar at the bed greatly improved collar performance, and no scour was observed at the front and sides of the pier. The deepest scour hole was at the collar edge, with a depth similar to the maximum scour depth in the experiment of a hooked-collar placed at 0.25b above the bed. This finding is similar to observations by Kumar et al. [13]. Their study used a collar of diameter 4.0b, which is much larger than that of the hooked-collar and which may not be practical in practice. To reduce construction cost, using a hooked-collar may achieve similar performance to a collar with a large width.

![Figure 5. Observed scour pattern around the piers: (a) bridge pier without the hooked-collar; (b) pier with the hooked-collar positioned 0.25b above bed; and (c) pier with the hooked-collar positioned at bed level.](image-url)
4.2. Numerical Results

FLOW-3D was employed to simulate local scour around five configurations of a hooked-collar, including three validation cases; no collar, single hooked-collar at 0.25b and a single hooked-collar at the bed level (Figure 4). In all the configurations, an attempt was made to ensure similar properties as the counterparts used in laboratory investigations. In addition, parameters used for validation in FLOW-3D were used to simulate other collar configurations. In each computation, the simulation lasted two days in an i7 7700k, 4.2 GHz, 4 cores, 8 logical processors and 64 GB of installed memory. It is well documented that the horseshoe vortex is one of the key processes by which scour around piers develops [11,23,30]. The Q criterion method, which defines a vortex as a connected fluid region of the positive invariant of velocity gradient tensor (\( \nabla u \)) [31], was used. In the formulation, the vorticity magnitude (\( \Omega \)) prevailed over the magnitude of the strain rate (\( S \)). This method signifies that the pressure in the vortex region was lower than the neighboring pressure.

\[
Q = \frac{1}{2} (\|\Omega\|^2 - \|S\|^2) > 0
\]  

(1)

Identified vortices are shown in Figure 6. Mounting the hooked-collar at 0.25b showed a similar vortex system to the no collar condition. Vortices were seen inside the scour holes in front of the cylinder (Figure 6a,b). The hooked-collar in Figure 6b weakened the vortex; moreover, the coherent structure was reactivated below the collar, a condition attributed to the scour pattern similarity. Conversely, these structures were blocked by the presence of hooked-collars at the bed level, thus minimizing the scour hole depth (Figure 6c,d).

Figure 6. Visualization of vortices: (a) no hooked-collar; (b) single hooked-collar at 0.25b; (c) single hooked-collar at bed level; and (d) double collar at the bed and buried 0.25b.
Computed streamlines are shown in Figure 7. Downflow in front of the cylinders is visible and its interception also shown where collars are placed at the bed surface. In front of the pier with no collar and a pier fitted with a hooked-collar placed 0.25b above the bed, a single near-bed velocity stagnation was observed, and this was caused by the horseshoe vertex illustrated in Figure 6 and incoming flow. On the contrary, velocity stagnation in piers fitted with collars occurred within the collar, thus preventing any scour in front of the pier. Interception of the intense downflow in front of the pier was clearly demonstrated by the streamlines.

![Streamlines Visualization](image)

Figure 7. Visualization of streamlines: (a) no hooked-collar; (b) single hooked-collar at 0.25b; (c) single hooked-collar at bed level; and (d) double collar at the bed and buried −0.25b.

Figure 8 shows bed elevation contours. By observing the scour patterns, the scour shape around the bridge-pier with or without a hooked-collar were similar (Figure 5). Scour patterns were similar under no hooked-collar and collar attached at 0.25b above the bed level (Figure 8a,b). Likewise, similar patterns were observed when the collar was placed at the bed level (Figure 8c,d). Maximum scour was on the sides in the latter configuration, while in the former, scour was almost around the pier. In all cases, the scouring patterns were almost symmetrical along the center of the channel in the x direction with the exception of deposition downstream of the pier. The model in all simulated cases underestimated deposition. In addition, deposition occurred farther from the pier without a hooked-collar, differing from observed patterns, as is shown in Figure 5.
Figure 8. Contours of scour depth: (a) no hooked-collar; (b) single hooked-collar at 0.25b; (c) single hooked-collar at bed level; and (d) double collar at the bed and buried −0.25b.

Figure 4 shows scour development (dimensionless scour, $d_s/b$) at the maximum scour region in the simulated tests. The results of FLOW-3D at every 10 s was used to produce this figure. As illustrated in Figure 8, the maximum scour occurred in mainly two regions; at the front of pier in the case of the no collar pier, while it was on the sides when a hooked-collar was attached. At the early stage, the scour rate was largest when there was no collar attached followed by a single collar attached at 0.25b. In both cases, the rate increased quickly and reduced before reaching an equilibrium $d_s/b$ of 0.83 and 0.63 at about 100-s and 160-s simulation time, respectively for the no collar and a single hooked-collar at 0.25b. Contrary to these configurations, when a hooked-collar was attached at the bed level or in a double collar condition, the scour rate was gradually increased, followed by a brief sharp increase, after which an equilibrium state was attained. Overall, the final scour depth was lowest when double collars were applied (a decrease of 50% from the pier without collar), one at the bed level and another installed at −0.25b from the bed. Moreover, in practice, a single collar may be enough considering the insignificant difference between a single and a double collar-fitted pier. Additionally, in real rivers, the live-bed scour condition exists where sediment load approaching the pier may be added in to the scour hole [32]. This suggests that the sharp increase in scour development seen in Figure 4 may be even less significant in a field setup.
5. Conclusions

In this study, a hooked-collar that aims to reduce traditional collars is presented. Laboratory experiments and numerical methods were applied to evaluate the performance of the hooked-collar. To find its optimum placement at the bridge pier, \(0.25b\) vertical adjustment was implemented. A hooked-collar placed at \(0.25b\) under the channel bed reduced the maximum scour depth by 24%. With a single hooked-collar placed at the bed level, the final scour depth was reduced 42%, while a double collar, at the bed and \(0.25b\) above the channel bed had the largest scour rate reduction of 50%. During the initial scouring stages, the scouring rate increase was rapid with this configuration, a similar pattern observed under the cylinder without any collar attached. Bed scouring simulated by FLOW-3D was slightly above measured scour depths; moreover, the model captured well the maximum time-dependent scour depth, as this was similar to observed flume experiments.

6. Patents

A United States Patent Number US7823240B2, entitled Hooked-Collar for Piers and Bridge Including the Same, resulted from this work.

Supplementary Materials: The following are available online at http://www.mdpi.com/2073-4441/10/9/1251/s1.

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Abbreviations

The following abbreviations are used in this manuscript:

- \(b\): pier diameter
- \(w\): hooked collar width
- \(h\): hooked collar height
- \(d_s\): scour depth
- \(d_{50}\): medium grain diameter
- \(d_{84}\): grain size for which 84% of the bed is finer
- \(d_{16}\): grain size for which 16% of the bed is finer
- \(H\): flow depth
- \(k\): turbulent kinetic energy
- \(u\): time averaged streamwise velocity
- \(v\): time averaged transverse velocity
- \(w\): time averaged vertical velocity
- \(\sigma_g\): geometric standard deviation
- \(g\): gravity acceleration (m s\(^{-2}\))
- \(\Omega\): vorticity magnitude
- \(S\): strain-rate magnitude

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