Point–like gamma ray sources as signatures of distant accelerators of ultra high energy cosmic rays

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We discuss the possibility of observing distant accelerators of ultra high energy cosmic rays in synchrotron gamma rays. Protons propagating away from their acceleration sites produce extremely energetic electrons during photo-pion interactions with cosmic microwave background photons. If the accelerator is embedded in a magnetized region, these electrons will emit high energy synchrotron radiation. The resulting synchrotron source is expected to be point-like, steady and detectable in the GeV–TeV energy range if the magnetic field is at the nanoGauss level.

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Cosmic rays (CR) are observed up to energies beyond $10^{20}$ eV. Even though it is commonly believed that particles with energies up to $\sim 10^{15}$ eV are accelerated in supernova remnants, we are still far from having a clear picture of the origin of higher energy particles. In particular, the Ultra High Energy Cosmic Rays (UHECR) observed at the end of the spectrum constitute a real challenge for theoretical models, since their acceleration requires extreme conditions that can hardly be fulfilled by known astrophysical objects. Previous studies have considered a number of potential sources, including gamma ray bursts, active galactic nuclei, large scale jets and neutron stars, but results are still inconclusive.

Moreover, even if some astrophysical objects accelerate UHECRs, a suppression, known as the Greisen-Zatsepin-Kuzmin (GZK) cutoff, should be observed in the CR spectrum at an energy $E_{\text{GZK}} \sim 7 \times 10^{19}$ eV, if UHECR sources are homogeneously distributed in the Universe. This is because during propagation energetic protons undergo $p\gamma$ interactions (mainly photo-pion production) in the Cosmic Microwave Background (CMB) photon field, with an energy loss length which decreases dramatically from $\sim 650$ to $\sim 20$ Mpc between energies of $7 \times 10^{19}$ to $3 \times 10^{20}$ eV. The detection of a number of events above $E_{\text{GZK}}$ raised interest in non-acceleration models that involve new physics and do not require the existence of a cutoff in the spectrum. However, the issue of the presence or absence of the GZK feature is still debated. In the following we assume that astrophysical objects capable of accelerating UHECRs do exist and we discuss a possible way to identify them.

If UHECRs are not appreciably deflected by the intergalactic magnetic field (for a different view see [2]), their arrival directions should point back to the actual position of their accelerators. In principle, this fact could be used to identify accelerators located at a distance smaller than the proton loss length, that constitutes a sort of horizon for CRs. The interactions between protons and CMB photons, responsible for the existence of this horizon, also generate secondary gamma rays and electron-positron pairs (hereafter we refer to both electrons and positrons as electrons) that in turn start an electromagnetic cascade in the universal photon background. Low energy electrons produced in the cascade are effectively deflected by the intergalactic magnetic field, and their radiation would appear to a distant observer as an extended gamma ray halo. However, if the magnetic field close to the accelerator is at the nG level, first generation electrons generated during $p\gamma$ interactions cool rapidly by emitting GeV synchrotron photons and the development of the cascade is strongly inhibited.

We discuss the possibility to detect this synchrotron radiation from UHECR accelerators. Such a possibility is of great interest because of the following reasons. Both the synchrotron emitting electrons and parent protons are extremely energetic and not appreciably deflected by the intergalactic magnetic field, at least on the first Mpc distance scale. For this reason, the observed radiation is expected to be point-like, and thus easily detectable and distinguishable from the extended cascade component. Remarkably, a possible detection of these sources would allow us to infer the value of the intergalactic magnetic field close to the accelerator, constraining it in the range between a fraction and a few tens of nG. Finally, since the Universe is transparent to GeV photons, also powerful UHECR accelerators located outside the CR horizon might be identified in this way.

Synchrotron gamma rays.– Consider a steady and isotropic accelerator of UHECRs. The actual nature of the accelerator as well as the details of the mechanism through which protons are accelerated up to ultra high energies are irrelevant for the discussion here. The only assumption we make is that protons with energies up to $10^{20}$ eV and beyond can leak out of the acceleration region and propagate away. In a mildly magnetized environment, such energetic protons follow almost rectilinear trajectories up to a distance roughly equal to the proton loss length. For proton energies greater than $\sim 5 \times 10^{19}$ eV the most relevant loss channel is photo-pion production in interactions with CMB photons and the loss length is $\lambda \sim 150$ Mpc at $10^{20}$ eV and rapidly decreases at higher energies. This implies that, if the accelerator is located
at a distance much greater than \( \lambda \), it cannot be directly observed as a source of UHECRs.

During photo-pion interactions both neutral and charged pions are produced. They in turn decay giving as final products photons, electrons and neutrinos. If \( E_{p,20} \) is the energy of the incoming proton in units of \( 10^{20}\) eV, the typical energy of the outgoing photons, electrons and neutrinos are \( E_\gamma \sim 10^{19}E_{p,20}\) eV and \( E_{e,\pm} \sim E_\nu \sim 5 \times 10^{18}E_{p,20}\) eV respectively. Electrons and photons interact via Compton and pair production processes with soft photons in the CMB and radio background. In general, this would lead to the development of an electromagnetic cascade, in which the number of electrons and photons increases rapidly. In fact, due to the extremely high energy of the particles considered here, each interaction occurs in the limit \( \epsilon_b E \gg 1 \), where \( \epsilon_b \) and \( E \) are the energies of the background photons and of the energetic electron (or photon) respectively, both calculated in units of the electron rest mass energy. Under this condition the Compton scattering is in the extreme Klein-Nishina limit, namely, the upscattered photon carries away most of the energy of the incoming electron. The same happens during a pair production event, in which most of the energy goes to one of the two outgoing electrons. The fraction of the energy lost by the energetic particle is approximately \( f \sim 1/\ln(2\epsilon_b E) \), which reduces to only a few percent if we consider a \( 10^{19}\) eV electron interacting with a CMB photon. Therefore the problem reduces essentially to a single-particle problem, in which a leading particle loses continuously energy and changes state from electron to photon and back: \( e^\pm \to \gamma \to e^\pm \ldots \) due to alternate Compton and pair production interactions. Thus, the effective loss length for an energetic electron can be identified with the loss length of the leading particle [11].

If a magnetic field \( B \) is present close to the accelerator, electrons also lose energy via synchrotron emission. In Fig. 1 we show the effective electron loss length calculated following [11] (solid line), together with the synchrotron loss length for different values of the magnetic field strength (dashed lines, 0.1, 1 and 10 nG top to bottom). Above a certain energy \( E_* \), synchrotron losses dominate over Compton/pair production ones. If we assume that the magnetic field is \( 1 \) nG, then \( E_* \sim 10^{18}\) eV and the energy of the synchrotron photons falls in the GeV range: \( E_{\text{syn}} \sim 10[B/(\text{nG})][E/(10^{19}\text{eV})]^2 \text{GeV} \). This implies that the presence of UHECR accelerators could in principle be revealed by means of gamma ray observations.

A necessary condition for the production of synchrotron photons is that the size of the magnetized region surrounding the accelerator must be greater than or comparable with the interaction length of UHECR protons. Thus, we consider here a region of size \( \sim 10 \) to \( 20\) Mpc, large enough to allow effective electron production inside the magnetized environment. Superclusters of galaxies constitute an example of a very large and appreciably magnetized region satisfying our requirement [12]. It is important to stress that our results are sensitive only to the value of the magnetic field close to the UHECR source, while they are unaffected by the value of the field on much larger scales.

**Angular size.** A mild magnetic field close to the source can slightly deflect UHECRs. Adopting the small scattering-angle approximation and neglecting energy losses, an order of magnitude estimate of the deflection angle for a proton of energy \( E \) propagating in a magnetized region of size \( d_p \): \( \vartheta_p \sim 1^{\circ}(10^{20}\text{eV}/E)(B/\text{nG})\sqrt{(d_p/20\text{Mpc})/(l_c/\text{Mpc})} \), where \( l_c \) is the magnetic field coherence length [13]. A fraction of the protons undergoes \( p\gamma \) interactions before escaping the magnetized region, producing extremely energetic electrons. If the magnetic field is at the \( nG \) level, electrons with energy in excess of \( \sim 10^{18}\) eV cool fast via emission of synchrotron gamma rays, depositing all their energy along the direction of their motion. This implies that an observer at a distance \( D \) would see a gamma ray source with angular size \( \vartheta_{\text{obs}} \leq 2\vartheta_p(d_p/D) \sim 3'(\text{Gpc}/D) \). This leads to the important conclusion that, even if the gamma rays are produced in an extended region of size \( d_p \sim 20\) Mpc surrounding the accelerator, the source would appear point-like to a distant observer.

In particular, GLAST, whose angular resolution at energies in the range \( 1 \sim 10\) GeV is roughly a fraction of a degree, will classify these sources as point-like if they are located at a distance greater than \( D \sim 50 \sim 100\) Mpc. For Imaging Atmospheric Cherenkov Telescope arrays (IACT) operating at energies above \( 100\) GeV this minimum distance is \( \sim 1\) Gpc, since their angular resolution is of the order of a few arcminutes. Electrons with energy smaller than \( E_* \) are not affected by synchrotron losses and start an electromagnetic cascade, that in principle might be detected at TeV energies by IACTs [8]. How-

![FIG. 1: Effective loss length for electrons. Solid line refers to Compton and pair production processes in the CMB and radio background (assumed to have a low frequency cutoff at \( 2 \sim \text{MHz} \)). Dashed lines refer to synchrotron losses in a magnetic field of 10, 1 and 0.1 nG (curves 1, 2 and 3).](image-url)
We further assume $\delta = 2$, though results are quite insensitive to the slope of the CR spectrum.

In the top panel of Fig. 2 we fix $E_{\text{cut}} = 10^{21}\text{eV}$ and we consider three different values for the magnetic field: 0.5, 5 and 50 nG (curves 1, 2 and 3 respectively). If the magnetic field is significantly greater than $\sim 50$ nG, the peak of the emission falls at TeV energies, where absorption is very strong. The absorbed photons start an electromagnetic cascade that will appear as an extended halo. On the other hand, if the field is well below $\sim 0.5$ nG, synchrotron emission becomes unimportant and again the cascade contribution dominates. However, for the broad interval of values of the magnetic field strength between 0.5 and 50 nG, the formation of a synchrotron point-like gamma ray source seems to be unavoidable.

In the bottom panel of Fig. 2, our predictions are compared with the sensitivities of GLAST and of a generic IACT array such as HESS [15]. A magnetic field of 1 nG is assumed and the three different curves refer to values of the cutoff energy in the proton spectrum equal to $E_{\text{cut}} = 5 \times 10^{20}$, $5 \times 10^{21}$ and $5 \times 10^{22}\text{eV}$ (top to bottom). For such a magnetic field, the condition for the detectability of a point source by GLAST is roughly $L_{\text{UHE}} \geq 8 \times 10^{43} \pm 2 \times 10^{44}(D/100\text{Mpc})^2\text{erg/s}$ for $\delta$ in the range 2.0 $\pm$ 2.6. In contrast, for IACT arrays the minimum detectable luminosity is about 2 orders of magnitude higher, since the source has to be located at a distance of $\sim 1\text{Gpc}$ in order to appear point-like. Moreover, distant sources may be undetectable above 100 GeV due to the strong absorption in the infrared background. In this case, the maximum energy of UHECRs is very important, since it determines the extension of the gamma ray spectrum towards high energies. Since the peak of the emission falls at $\sim 10$ GeV, the future IACT arrays operating in the energy range $10 \div 100$ GeV would be powerful tools to search for these sources.

If the CR spectrum is a smooth power law with index $\delta = 2$ down to GeV energies, the required total CR luminosity for a source to be detected by GLAST is $L_{\text{CR}} \geq 5 \times 10^{44}(D/100\text{Mpc})^2\text{erg/s}$. If CRs are beamed along one axis, the luminosity is reduced by a factor $f_b \sim 0.02(\vartheta_b/10^\circ)$, $\vartheta_b$ being the beaming angle. In this case, the detectability condition reads: $L_{\text{CR}} \geq 10^{43}(f_b/0.02)(D/100\text{Mpc})^2\text{erg/s}$. This luminosity is small if compared, for example, with the kinetic power of an AGN jet, that can be as high as $\sim 10^{47}\text{erg/s}$ [18]. Thus, astrophysical object that could in principle satisfy the energy requirement for detectability do exist.

In calculating the spectra shown in Fig. 2 we assumed the UHECR accelerator to be active for a time $t_{\text{ON}}$ long enough to reach steady state. This situation is achieved if the accelerator lifetime is greater than the $\gamma \gamma$ interaction time, namely, if $t_{\text{ON}} \geq 100\text{Myr}$. Under this assumption, the total energy deposited in CRs during the whole source lifetime is $E_{\text{CR}} \geq 3 \times 10^{48}(f_b/0.02)(D/100\text{Mpc})^2\text{erg}$. If the UHECR accelerator is located inside a rich cluster of galaxies, then the bulk of this nonthermal energy accumulates in it, due to effective diffusive confinement of

![FIG. 2: Photon spectra for a source at a distance of 1Gpc in a 20Mpc magnetized region. The luminosity in UHECRs is $10^{46}\text{erg/s}$, the proton spectral index is $\delta = 2$. TOP: $E_{\text{cut}} = 10^{21}\text{eV}$, magnetic field 0.5 (curve 1), 5 (2), 50 nG (3). BOTTOM: $E_{\text{cut}} = 5 \times 10^{20}, 5 \times 10^{21}, 5 \times 10^{22}\text{eV}$, magnetic field is 1nG. Dotted lines represent the intrinsic spectra, solid lines show the effect of absorption in the infrared background. The sensitivities of GLAST and of a generic IACT are shown.](image-url)
CRs with energy up to at least $10^7\text{GeV}$ in the $\mu$G intracluster magnetic field. Such an amount of energy can be easily stored in a rich cluster, whose total thermal energy can be as high as $10^{64}\text{erg}$.

Of course, if the CR spectrum is much steeper than $\delta = 2$, the problem of energetics could be difficult to circumvent, unless a mechanism is found to limit acceleration to ultra high energy particles only.

Thus, calculations show that for objects located within several hundreds of megaparsecs and with jets pointed to the observer, GLAST and Cherenkov telescopes like HESS should be able to provide meaningful probes of this radiation. Distant objects beyond 1 Gpc will be possibly detected only by the next generation instruments with significantly improved sensitivities.

**Bursting sources.**—The results presented above can be qualitatively generalized to the case of a bursting source. Consider a short burst releasing an energy $E_{\text{burst}}^{\text{UHE}}$ in the form of UHECRs. The deflection of UHECRs in magnetic fields results in a time broadening of the pulse over a time roughly equal to the delay time $\delta t \sim 5\times10^5(E_{\text{burst}}^{\text{UHE}}/E)^2(B/nG)^2(d_p/20\text{Mpc})^2(l_c/\text{Mpc})\text{yr}$. The duration of the synchrotron emission is expected to be roughly the same. If the intrinsic duration of the burst $t_b$ is longer than $\delta t$, time broadening is not important. To satisfy the detectability condition, the total energy released in UHECRs must be $E_{\text{burst}}^{\text{UHE}} \geq L_{\text{UHE}}^{\text{obs}} t_{\text{obs}} \sim 2\times10^{53}(t_{\text{obs}}/\delta t)(f_b/0.02)(D/100\text{Mpc})^2\text{erg/s}$ where $L_{\text{UHE}}^{\text{obs}}$ is the detectability condition for the steady state situation and $t_{\text{obs}} \sim \delta t + t_b$ is the observed duration of the burst. This is a huge amount of energy to be released in a single explosion, orders of magnitude above the energy $\sim 10^{51}\text{erg}$ that is believed to be converted into UHECRs during a gamma ray burst. Thus, if UHECRs are produced during short bursts, the related synchrotron emission is far too faint to be detected. However, if the accelerator remains active for a time $\gg \delta t$ the energy requirement is significantly reduced.

**Neutrinos.**—Muon and electron neutrinos are produced during $p\gamma$ interactions in the ratio 2:1. Due to neutrino oscillation the ratio between the three flavors becomes 1:1:1 at Earth. For the source considered in Fig. 2 the total neutrino flux is $E^2\nu \sim 1\text{EeV}/\text{km}^2/\text{yr}$ at energy $5\times10^8\text{eV}$. These energies will be probed by the ANITA and AUGER experiments. The possibility of a detection will depend on their performances in recognizing steady point sources. The detection of neutrinos could serve as an unequivocal signature of UHECR acceleration. The authors thank S. Barwick, P. Blasi, P. Coppi, C. Ferrigno, J. Hinton and E. Resconi for useful discussions. SG acknowledges support from the Humboldt Foundation.

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22. If CRs are accelerated only above an energy $E_{\text{min}}$ then $L_{\text{CR}} \propto E_{\text{min}}^{-3}/(\delta - 2)$. For a steep spectrum $\delta = 2.6$ and $E_{\text{min}} = 1\text{GeV}$ the required luminosity is huge $L_{\text{CR}} \sim 2.4 \times 10^{30}\text{erg/s}$. 
