STATISTICAL SEARCHES FOR MICROLENSING EVENTS IN LARGE, NON-UNIFORMLY SAMPLED TIME-DOMAIN SURVEYS: A TEST USING PALOMAR TRANSIENT FACTORY DATA

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ABSTRACT

Many photometric time-domain surveys are driven by specific goals, such as searches for supernovae or transiting exoplanets, which set the cadence with which fields are re-imaged. In the case of the Palomar Transient Factory (PTF), several sub-surveys are conducted in parallel, leading to non-uniform sampling over its ∼20,000 deg2 footprint. While the median 7.26 deg2 PTF field has been imaged ∼40 times in the R band, ∼2300 deg2 have been observed >100 times. We use PTF data to study the tradeoff between searching for microlensing events in a survey whose footprint is much larger than that of typical microlensing searches, but with far-from-optimal time sampling. To examine the probability that microlensing events can be recovered in these data, we test statistics used on uniformly sampled data to identify variables and transients. We find that the von Neumann ratio performs best for identifying simulated microlensing events in our data. We develop a selection method using this statistic and apply it to data from fields with >10 R-band observations, 1.1 × 109 light curves, uncovering three candidate microlensing events. We lack simultaneous, multi-color photometry to confirm these as microlensing events. However, their number is consistent with predictions for the event rate in the PTF footprint over the survey’s three years of operations, as estimated from near-field microlensing models. This work can help constrain all-sky event rate predictions and tests microlensing signal recovery in large data sets, which will be useful to future time-domain surveys, such as that planned with the Large Synoptic Survey Telescope.

Key words: gravitational lensing: micro – methods: statistical – surveys

Online-only material: color figures

1. INTRODUCTION

Over the past two decades, microlensing, in which gravitational lensing causes a transient increase in the flux from a background point source, has been used to search for dark and compact objects (Alcock et al. 1993; Osłowski et al. 2008; Saritore & Treves 2010), to study Galactic structure and kinematics (Binney et al. 2000), to determine the shape of stars (Rattenbury et al. 2005), and to identify extrasolar planets (Gaudi 2011 and references therein). Such studies were once limited by the small number of detected events, but thanks to advances in CCD technology and the development of dedicated microlensing surveys, a few thousand events are now observed each year.8 In the coming decade, this number is expected to increase as the next generation of photometric, time-domain surveys comes online, providing an opportunity for the precise study of otherwise hard-to-characterize objects such as low-mass stars, sub-stellar objects, and isolated neutron stars.

Microlensing surveys typically focus on high-density stellar regions, such as the Galactic bulge, M31, or the Magellanic Clouds (e.g., Udalski et al. 1992; Alcock et al. 1993; Aubourg et al. 1993; Crotts & Tomane 1996), but microlensing events are not limited to dense stellar fields. Indeed, lensing events away from these fields are potentially very interesting. While the microlensing event rate in low-density stellar regions will be smaller compared with events found by modern microlensing surveys, these are expected to involve closer sources and lenses and less crowded backgrounds (Di Stefano 2008b). Thus, such lenses offer more opportunities to constrain the properties of the events.

Only one event outside of a dense stellar field has been recorded to date: the Tago event (Fukui et al. 2007; Gaudi et al. 2008), a serendipitous detection of the microlensing of a bright source. Gaudi et al. (2008) set probabilistic limits on the mass, distance, proper motion, and magnitude of this lens using existing observations near the event’s location and further observations may turn these limits into precise measurements. Such an analysis is usually not possible for events in high-density fields where the lenses are, on average, much farther away and blending makes photometry—and, therefore, mass measurements—challenging. In contrast, high Galactic latitude events probe lenses with distances ≲1 kpc; the Einstein radii, therefore, tend to be larger (~milliarcseconds) and may cause detectable astrometric signatures (Han 2008; Di Stefano 2008a, 2008b). A measurement of the astrometric shift due to microlensing will break the distance–mass degeneracy in the lensing parameters and enable a direct measurement of the lens mass. Finding even a handful of nearby lenses that can be studied in the same kind of detail as the Tago event would, therefore, be very valuable.

In this paper, we use the Palomar Transient Factory (PTF) survey, described in Section 2, as a test case for studying
the frequency and detectability of microlensing events in all-sky, irregularly sampled, time-domain surveys. Although to date no microlensing event has been reported using PTF data, a simple extrapolation from previous all-sky rate estimates suggests $\sim$1–10 detectable microlensing events within the PTF footprint over the survey’s three years of operation (Gaudi et al. 2008; Han 2008). We examine the selection methods used by microlensing surveys to identify event signatures in light curves as well as an event identification procedure based on a set of variability statistics. We then present the detection efficiency for these methods as computed for a representative set of PTF fields (Section 3). In Section 4, we apply a set of criteria that use the results of these tests to all PTF light curves with $>10$ high-quality observations to identify candidate microlensing events. We discuss eight interesting transients and three candidate events identified in this manner before concluding in Section 5.

2. PTF: SURVEY DESIGN AND CONSEQUENCES FOR MICROLENSING SEARCHES

PTF data are collected using the former Canada–France–Hawaii Telescope 12 K $\times$ 8 K mosaic camera, which has 11 working chips, 0.92 $\times$ 10$^5$ pixels, and a 7.26 deg$^2$ field of view (Rahmer et al. 2008), mounted on the 48 inch Oschin Schmidt Telescope at Palomar Observatory in California. Under median seeing conditions (2.2'), observations in Mould R or Sloan Digital Sky Survey (SDSS; York et al. 2000) g achieve 2'0 FWHM images and reach 5$\sigma$ magnitudes of $R \approx 21.0$ and $g \approx 21.3$ mag in each 60 s exposure (Law et al. 2009; Rau et al. 2009; Law et al. 2010).

While a real-time image-differencing pipeline identifies transients of interest and passes these to a dedicated photometric follow-up telescope, a separate pipeline generates PTF light curves. Images are processed using standard reduction procedures including de-biasing, flat-fielding, and astrometric calibration (R. Laher et al., in preparation). SExtractor is used for source identification (Bertin & Arnouts 1996). The absolute photometric calibration of the images is good to a systematic limit of $\sim$2% for photometric nights, as described in Ofek et al. (2012). The final light curves are produced using relative photometric calibration, which refines the calibration to $<1\%$ for photometric nights and improves the calibration for bad nights (D. Levitan et al., in preparation; for algorithm details, see Levitan et al. 2011; Ofek et al. 2012). The resulting archive is an excellent resource for the study of periodic forms of variability (e.g., stellar or asteroid rotation; Agüeros et al. 2011; Polishook et al. 2012).

As of 2012 December, the PTF footprint includes $\sim$15,224 (2766) deg$^2$ imaged $>10$ (>100) times in R band and $\sim$5430 (290) deg$^2$ imaged that often in g band (see Figure 1). The PTF survey footprint is not uniformly sampled either spatially or temporally. Each field has a unique sampling pattern determined by which of the PTF sub-surveys it belongs to, what time of the year it is visible, and how high a priority it is given by the scheduler. The imaging cadences range from one to five days, but other cadences are possible: for example, there was a higher-cadence campaign of a field in Orion to find transiting planets around young stars (van Eyken et al. 2011). The result is that PTF light curves often contain gaps and regions of high-cadence observations and/or low-cadence observations, so that the archive is a massive data set of irregularly sampled, time-domain photometry. Figure 2 shows six randomly selected light curves and illustrates the varying cadences and coverage that different fields may have over the same one year period. While the PTF database is not yet public, we have made $\sim$10$^4$ randomly selected light curves available at http://dx.doi.org/10.7916/D8CF9N1N. These light curves meet the quality criteria described in Section 3.2 and can be used to test the statistical methods described here (or others!).

In Figure 3, we plot the number of R-band exposures for each field against the observational baseline (the number of days between the first and last exposure). Given the exposure distribution, which peaks at 30–40 but includes a long tail to larger numbers, we restrict our sample to the light curves with $>10$ R-band observations.

3. MICROLENSING EVENT RECOVERY

Microlensing surveys typically use difference image analysis (Alard & Lupton 1998) to identify transient events in raw imaging data. The light curves of transient sources are then analyzed and vetted using a variety of selection methods to search for microlensing event candidates and distinguish them from, e.g., variable stars, outbursting systems, and novae. Surveys have approached this process differently (as described in Udalski et al. 1994; Wozniak 2000; Alcock et al. 2000, 2001;
The Astrophysical Journal, 781:35 (12pp), 2014 January 20

Price-Whelan et al.

Figure 2. Sampling of six different PTF fields over the course of a year. Darker points indicate that more exposures were taken that night; the total number of observations for each field is indicated.

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Udalski 2003; Hamadache et al. 2006; Wyrzykowski et al. 2009; Sumi et al. 2011), but the general idea is to require that
1. any selected light curve has some number of consecutive data points brighter than some threshold;
2. compared with flat or linear light-curve models, a microlensing model best describe the data; and
3. the microlensing model event parameters have physically reasonable values.

What would a microlensing event look like in a typical PTF light curve? If the source is an unblended point source and the lens is a foreground, dim object, a microlensing event is fully described by three parameters: the angular impact parameter $u_0$, the peak time of the event $t_0$, and the timescale of the event (the Einstein crossing time) $t_E$. In terms of a dimensionless projected distance between the source and lens (in units of Einstein radius), $u$, the amplification factor $A$ and flux $F$ as a function of time can be defined as

$$u(t) = \sqrt{u_0^2 + 2 \left( \frac{t - t_0}{t_E} \right)}.$$  

$$A(t) = \frac{u^2 + 2}{u \sqrt{u^2 + 4}}.$$  

$$F(t) = A(t) \times F_{\text{source}}.$$  

(Paczynski 1986). The microlensing perturbation can also be expressed as

$$m(t) = m_0(t) - 2.5 \log A(t),$$

where $m_0(t)$ is the unperturbed, but possibly time-variable, magnitude of the source.

Even in cases of high amplification ($u_0 \ll 1$), a survey may miss or poorly sample an event if $t_E$ is short ($t_E \lesssim$ days), while if $t_E$ is long ($t_E \gtrsim 1$ yr) the event may be confused with other forms of long-duration variability. Figure 4 illustrates the effect of simulated microlensing events with a fixed $t_E = 20$ days, but different angular impact parameter, $u_0$, on a random well-sampled PTF light curve.

Applying the standard microlensing-search prescription to the PTF data presents obvious challenges. For example, microlensing surveys have relatively uniform time sampling of their survey footprint over an observing season, justifying the first requirement. However, it is harder to motivate such a cut on data with significant and irregular gaps. In order to develop the most successful procedure for PTF data, we therefore examine the relative performance of a set of variability indices and the traditional prescription in selecting simulated microlensing events.

3.1. The Variability Indices

We choose five statistical measures of variability compiled by Shin et al. (2009) that have been previously applied to the classification and discovery of periodic variables. These variability indices are $\sigma/\mu$, Con, $\eta$, $J$, and $K$. $\sigma/\mu$ is the ratio of the sample standard deviation ($\sigma$) to the sample mean ($\mu$):

$$\frac{\sigma}{\mu} = \sqrt{\frac{\sum_{i=1}^{N} (x_i - \mu)^2}{(N-1)}} \quad \sqrt{\frac{\sum_{i=1}^{N} x_i^2}{N}},$$

where $N$ is the total number of observations.

We modify the definition of Con to be the number of clusters of three or more consecutive observations that are more than $3\sigma$ brighter than the reference magnitude of the source (e.g., for a single microlensing event in an otherwise flat light curve, $Con = 1$). This change allows us to use the performance of

9 We do not implement the sixth index described by Shin et al. (2009), AoVM, because it mainly helps identify periodic sources.
Figure 4. Simulating the effect of 20 day microlensing events with impact parameters $u_0 = 1.0, 0.5, \text{ and } 0.01$, on a random PTF $R$-band light curve. The original light curve is shown at the top. The dashed line in the bottom panel shows the approximate saturation limit of the PTF camera in the $R$ band; such an event with a brighter source might therefore be missed by the survey. (A color version of this figure is available in the online journal.)

Con as a proxy for the consecutive-point requirement described above.

$\eta$, the von Neumann ratio (also known as the Durbin–Watson statistic; von Neumann et al. 1941; Durbin & Watson 1950), is the mean square successive difference divided by the sample variance:

$$\eta = \frac{\delta^2}{\sigma^2} = \frac{\sum_{i=1}^{N-1} (x_{i+1} - x_i)^2}{(N - 1) \sigma^2}.$$  (6)

$\eta$ is small when there is strong positive serial correlation between successive data points.

$J$ and $K$ were suggested by Stetson (1996):

$$\delta_i = \sqrt{\frac{N}{N - 1}} \frac{x_i - \mu}{e_i},$$  \hspace{1cm} (7)

$$J = \frac{1}{N} \sum_{i=1}^{N-1} \text{sign}(\delta_i \delta_{i+1}) \sqrt{|\delta_i \delta_{i+1}|},$$  \hspace{1cm} (8)

$$K = \frac{1}{N} \sum_{i=1}^{N} |\delta_i| \sqrt{1/N \sum_{i=1}^{N} \delta_i^2}.$$  \hspace{1cm} (9)

where $e_i$ is the photometric error of each data point and the sign function returns ±1, depending on the sign of the argument. $J$ tends to 0 for non-variable stars, but is large when there are significant differences between successive data points in a light curve. $K$ is a measure of the kurtosis of the distribution of data points. We add one more index, $\Delta \chi^2$, the difference in $\chi^2$ between fitting a Gaussian model and fitting a linear model to a light curve. This is a standard statistical test used by microlensing surveys and allows us to compare the relative performance of the (slightly modified) Shin et al. (2009) indices and this approach.

Specifically, we use a Levenberg–Marquardt optimizer to perform a least-squares fit with each of these models to the light curves and then compute $\Delta \chi^2 = \chi_{\text{linear}} - \chi_{\text{gaussian}}$. Our tests with $\Delta \chi^2$ below compare the distribution of values over light curves on the same chip. As a result, the number of data points and number of model parameters are constant and we therefore do not include an Akaike or Bayesian information criterion term. For the Gaussian fit, the optimizer is initialized with a $\sigma$ of 10 days, centered on the brightest data point.

Figure 5 shows maximally outlying light curves for each variability statistic selected from $\sim$20,000 light curves for objects on a single CCD in PTF field 3756. Clearly, the indices are sensitive to different aspects of variability in the data. We expect $\sigma/\mu$ to be most useful for discerning periodic or semi-periodic variability where the variance is large; the expectations are not as clear for other indices.

We conduct Monte Carlo simulations and inject artificial microlensing events into real PTF light curves. We then compare the distributions of variability indices for a set of light curves with and without these simulated events to determine the regions
3.2. Event Selection and Detection Efficiency

We begin by randomly sampling 1000 light curves from each chip in a given PTF field. At least half of the individual observations in these light curves must be defined as “good” (see the description of the processing pipeline in Law et al. 2009). The rejected light curves are for objects that are either faint or near bright stars whose scattered light and diffraction spikes cause large photometric errors.

For each of these light curves, we use the date and magnitude error information to simulate 100 light curves with purely Gaussian scatter. We find the value of each variability index such that the selection using that index to identify interesting light curves returns 1% of these scrambled light curves—i.e., we set the limiting value of each index such that the false positive recovery (FPR) rate is 1% per trial. We again randomly sample 1000 light curves from each CCD with > 10 good observations and compute the set of indices for these light curves. Finally, we add 100 different simulated microlensing events to each light curve and evaluate how often these events are recovered given the 1% FPR cut defined above.

The parameters for each simulated event are chosen as follows: $t_0$ is drawn from a uniform distribution between the first and last observation date, $u_0$ is drawn from a uniform distribution between 0 and $\sim 1.5$ (the impact parameter that causes a maximum deviation larger than $\sim 5\sigma$ for a $R \sim 17.5$ mag source; e.g., Alcock et al. 2001), and $t_E$ is drawn from a log-uniform distribution between 1 and 1000 days. For each
iteration, we recompute the variability indices and store the event parameters.

Figures 7–9 show the results for three representative fields with different sampling patterns (top panels) and detection efficiency curves computed using this simulation (bottom panels). We ignore the indices $K$ and $s/\mu$ because their integrated detection efficiencies are below 1%. At a fixed FPR of 1%, Con performs poorly, but it may be useful as an initial cut if a higher FPR is used. In this work, we only consider a single-index selection method and thus reject Con.

For each of these fields, we find that $\eta$ consistently performs better than the other indices at recovering microlensing events. This is especially interesting because computing $\eta$ is $\sim 100 \times$ faster per light curve than computing $\Delta \chi^2$. Identifying candidate microlensing events in the full PTF data set using this statistic is therefore computationally plausible.

4. SEARCHING FOR EVENTS IN THE FULL PTF DATA SET

To identify candidate microlensing events, we

1. select the light curves from one of the 2097 fields with >10 $R$-band observations;
2. identify those light curves with more than 50% good data points and >10 good observations and run Monte Carlo simulations to compute the 1% FPR limiting values for $\eta$, $\Delta \chi^2$, and $J$ for that field;
3. compute $\eta$ for all the light curves in the field (while $\sim 10\%$ of the light curves pass the quality cut described above, only $\sim 0.1\%$–$0.5\%$ of these survive the FPR cut determined from the Monte Carlo simulations);
4. for fields with SDSS coverage, we use Data Release 9 photometry (Ahn et al. 2012) to remove sources typed as Galaxy or quasi-stellar object (QSO; using objc_type$^{10}$) and flag candidate quasars (using the cuts described in Richards et al. 2002); this eliminates $\sim 90\%$ of the remaining light curves;
5. fit a microlensing event model and subtract the model, then recompute $\eta$ for all the selected light curves;
6. reject the light curves for which the new value of $\eta$ still passes the cut$^{11}$ – this step eliminates $\sim 90\%$–$95\%$ of the remaining light curves; and
7. retain any surviving light curves for further inspection (typically, there is $\lesssim 1$ such light curves per field).

$^{10}$ http://www.sdss3.org/dr9/algorithms/classify.php
$^{11}$ These are probably periodic variables.
This procedure identifies 2377 candidates from among the initial sample of $1.1 \times 10^9$ light curves. We search SIMBAD\textsuperscript{12} and remove any candidate among these with a known extragalactic counterpart within $10''$. For those in the SDSS footprint, we examine the SDSS images (Nieto-Sanisteban et al. 2004) to identify extended objects. Removing extragalactic objects in this manner from our candidate list reduces contamination by, e.g., supernovae.

We visually inspect each of the remaining $\sim 2000$ light curves. We identify an additional $\sim 1100$ objects with unknown long-term variability (e.g., Mira-type variables, quasars not in the SDSS footprint). An additional $\sim 600$ light curves have bad or poorly calibrated data that mimic a transient increase in flux: diffraction spikes, ghosts, and scattered light can cause non-Gaussian, seeing-dependent variability. Where appropriate, as an additional test, we examine the PTF images to verify the data quality. A small fraction of the light curves are variable stars that survived our periodic variability cut.

We are left with $\sim 300$ unclassified transients. Through visual inspection of these light curves, we classify the bulk of these as novae, supernovae, flares, or outbursting systems and identify 11 microlensing event candidates. We then search the literature for additional photometric data for these 11 objects. Most have a counterpart in Wide-field Infrared Survey Explorer (WISE; Wright et al. 2010), while a few have a counterpart in Two Micron All Sky Survey (2MASS; Cutri et al. 2003); see Table 1 for a summary. We also obtained spectroscopy for several of these candidates. Below, we detail what can be learned from these data. Generally, additional deeper optical/infrared imaging and/or optical spectroscopy is required to draw firm conclusions about the nature of the object.

To summarize what follows, we rule out five of the 11 candidates as being likely extragalactic transients based on photometry and/or imaging from WISE, 2MASS, and/or PTF. Three of the candidates are not detected in WISE and/or 2MASS; follow-up imaging or spectroscopy is needed to draw any conclusions about these objects. The remaining three objects (PTF1J061800.25+203242.5, J161502.39+540053.8, and J172826.08+692501.1) are likely stars and, given the observed PTF variability, plausible microlensing events. We emphasize, however, that lacking simultaneous, multi-color photometry during the events, we cannot claim these as microlensing events with any confidence. These three candidates are shown in Figure 10 and PTF cutouts of the associated sources at quiescence and near peak brightness are shown in Figure 11.

\begin{table}[h]
\centering
\caption{Photometric Properties of the Microlensing Candidates}
\begin{tabular}{lcccccccc}
 & PTF & $R$ & $(g' - R)$ & $J$ & $(J - H)$ & $(H - K)$ & W1 & $(W1 - W2)$ & $(W2 - W3)$ & $(W3 - W4)$ \\
\hline
J0335$^a$ & 18.28 $\pm$ 0.12 & --- & 16.59 $\pm$ 0.13 & 0.73 $\pm$ 0.18 & 0.79 $\pm$ 0.18 & 15.06 $\pm$ 0.04 & 0.18 $\pm$ 0.09 & --- & --- & --- \\
J0618 & 20.13 $\pm$ 0.10 & 1.13 $\pm$ 0.22 & 16.23 $\pm$ 0.09 & 0.77 $\pm$ 0.15 & 0.70 $\pm$ 0.15 & 14.08 $\pm$ 0.03 & 0.49 $\pm$ 0.05 & 3.22 $\pm$ 0.09 & 2.65 $\pm$ 0.19 \\
J1206$^b$ & 19.24 $\pm$ 0.27 & --- & --- & --- & --- & 15.37 $\pm$ 0.04 & 0.81 $\pm$ 0.06 & 2.46 $\pm$ 0.17 & 2.96 $\pm$ 0.37 \\
J1315 & 19.69 $\pm$ 0.28 & --- & --- & --- & --- & 16.20 $\pm$ 0.20 & $\pm$ 0.43 $\pm$ 0.21 & --- & --- \\
J1532$^b$ & 20.01 $\pm$ 0.24 & 1.10 $\pm$ 0.29 & --- & --- & --- & 16.36 $\pm$ 0.04 & 0.09 $\pm$ 0.11 & --- & --- \\
J1615 & 20.27 $\pm$ 0.20 & 0.17 $\pm$ 0.28 & --- & --- & --- & 15.56 $\pm$ 0.04 & 0.85 $\pm$ 0.07 & 2.93 $\pm$ 0.15 & --- \\
J1728 & 20.15 $\pm$ 0.23 & 0.00 $\pm$ 0.34 & 17.18 $\pm$ 0.21 & --- & --- & 13.92 $\pm$ 0.02 & 0.01 $\pm$ 0.03 & $\pm$ 0.28 $\pm$ 0.50 & --- \\
J1747$^a$ & 17.37 $\pm$ 0.10 & 0.20 $\pm$ 0.12 & 16.12 $\pm$ 0.07 & 0.49 $\pm$ 0.13 & 0.92 $\pm$ 0.13 & 13.10 $\pm$ 0.03 & 1.01 $\pm$ 0.03 & 2.96 $\pm$ 0.04 & 2.68 $\pm$ 0.06 \\
J1933$^b$ & 17.53 $\pm$ 0.10 & 1.13 $\pm$ 0.27 & 15.77 $\pm$ 0.07 & 0.74 $\pm$ 0.11 & 0.59 $\pm$ 0.13 & 14.16 $\pm$ 0.03 & 0.15 $\pm$ 0.04 & 0.94 $\pm$ 0.44 & --- \\
\end{tabular}
\end{table}

\textbf{Notes.} Objects in bold are plausible microlensing candidates.
\textsuperscript{a} Photometry and/or visual inspection of the PTF/WISE images rule these out as plausible candidate events.
\textsuperscript{b} Available data are insufficient to determine the likelihood that these are plausible candidate events.

\textsuperscript{12} This research has made use of the SIMBAD database, operated at CDS, Strasbourg, France.
For these three plausible events, we use a Markov Chain Monte Carlo algorithm (Goodman & Weare 2010; Foreman-Mackey et al. 2013) to derive posterior probability distributions over each parameter in the point-source, point-lens microlensing model (Equation (4)). Overplotted on Figure 10 are samples from these posterior distributions along with the maximum a posteriori (MAP) model; the corresponding MAP event parameters are listed in Table 2. The event durations for PTF1J0618 and PTF1J1615 are reasonable, given that a ~0.1 $M_\odot$ lens at ~500 pc in the thick disk ($\mu_{\text{tan}} \sim 50 \text{ km s}^{-1}$) has a typical event duration $t_E \sim 20$ days, but the significantly longer duration of PTF1J1728 (>150 days) could be a sign of a larger mass lens or larger distance.

### Table 2

| PTF1 | $u_0$   | $t_E$  | $t_0$  | $m_0$  | (days) | (MJD) | (R)   |
|------|---------|--------|--------|--------|--------|-------|-------|
| J0618| 0.178 ± 0.011 | 23.7 ± 1.6 | 55880.0 ± 0.4 | 20.222 ± 0.034 |
| J1615| 0.376 ± 0.016 | 31.4 ± 1.1 | 55895.5 ± 2.1 | 20.019 ± 0.004 |
| J1728| 1.338 ± 0.002 | 161.1 ± 4.9 | 55192.2 ± 1.4 | 16.260 ± 0.002 |

PTF1J0618 and PTF1J1728 have counterparts in 2MASS and we can therefore use the Covey et al. (2007) $J$-band absolute magnitudes for stars of the relevant spectral types to estimate rough distances to these stars, assuming they have solar metallicity (see below for a discussion of how we obtain spectral types for these stars). For PTF1J0618, this results in a distance that ranges from 1.1 kpc (if it is a M1 star) to 0.8 kpc (if it is a M3 star), corresponding to heights above the Galactic plane of 43 and 31 pc, respectively. For PTF1J1728, assuming it is a K0–K5 star results in distances ranging from 1.3 to 0.7 kpc and heights of 0.9 to 0.5 kpc.

We lack a spectrum for PTF1J1615, so the distance estimate to this star is even more uncertain. Still, we compare the PTF $R$ magnitude with the stellar library compiled by Pickles (1998) to estimate a distance, assuming (from its photometry) that it is a K5–M2 star. This results in distances ranging from 4.2 to 1.9 kpc and heights from 2.3 to 1.0 kpc. The estimated heights above the Galactic plane suggest that PTF1J0618 is a thin-disk star, while the other two, PTF1J1615 and PTF1J1728, are plausible thick-disk members (Bochanski et al. 2010).

### 4.1. Plausible Microlensing Candidates

PTF1J0618 is detected in 2MASS and in all four WISE filters. The corresponding colors are difficult to interpret, however: the object’s $(J - H)$ color is consistent with that of a mid-M dwarf (Covey et al. 2007), but its $(H - K)$ is significantly redder than expected for such a star. Meanwhile, PTF1J0618’s WISE colors suggest it is an extragalactic object (see Figure 14 in Yan et al. 2013). We observed PTF1J0618 for 1200 s with the Double Spectrograph (DBSP; Oke & Gunn 1982) on the Hale 5 m telescope at Palomar Observatory, California, on 2013 February 19; see Figure 12. The spectrum was obtained with the D55 dichroic; from the atmospheric cutoff to 5500 Å, the grating had 600 line mm$^{-1}$ and was blazed at 4000 Å, giving a resolution of 1.1 Å. From 6300–8800 Å, the grating was 158 line mm$^{-1}$, was blazed at 7500 Å, and gave a resolution of 2.5 Å. The data were reduced using standard IRAF routines.

13 This ignores differences between Mould and Cousins $R$ filters.

14 IRAF is distributed by the National Optical Astronomy Observatories, which are operated by the Association of Universities for Research in Astronomy, Inc., under cooperative agreement with the National Science Foundation.
We analyzed this spectrum with the HAMMER IDL package (Covey et al. 2007). The HAMMER measures a suite of spectral features and provides automated spectral types by comparison to templates. The typical uncertainty in HAMMER spectral typing is $\lesssim 1$ spectral subclass. PTF1J0618 is clearly an early M star, with a spectral type of M2–M3.

M stars are well-known sources of stellar flares and in sparse data these could easily be confused for a microlensing event. However, typical flares on M stars last minutes to hours, with the longest seen being of order eight hours (Kowalski et al. 2010). In contrast, the candidate event detected by PTF had a duration $\sim 30$ days and is therefore highly unlikely to have been a flare.

Could PTF1J0618 be an outbursting symbiotic star? To test this hypothesis, we compare the DBSP spectrum with a set of M1–M2 dwarf and giant star spectra. We inspect the depth of the Ca II triplet lines and also calculate several of the spectral indices collected by Covey (2006) to distinguish between dwarfs and giants (e.g., the fluxes in the Na D 5900 and CN 7900 bands). These all indicate that PTF1J0618 is a dwarf star, rendering it unlikely that the PTF event was a symbiotic-type outburst. We further note that those outbursts typically last $\sim$years (e.g., Tomov et al. 2013). We conclude that this is a plausible candidate microlensing event.

$PTF1J161502.39+540053.8$

PTF1J1615 is one of two candidates that fall in the SDSS footprint; its counterpart, SDSS J161502.43+540053.6, has a proper motion of 2.66 mas yr$^{-1}$, consistent with its automated SDSS classification as a star. The star has $u = 22.9$ mag$^{15}$ beyond the $u = 22.0$ 95% completeness limit for SDSS (Stoughton et al. 2002) and we therefore focus on its $griz$ photometry. With $(g - r) = 1.10 \pm 0.05$, $(r - i) = 1.00 \pm 0.03$, and $(i - z) = 0.56 \pm 0.04$, the star’s colors are consistent with those of a late K/early M star (Covey et al. 2007). PTF1J1615 has no counterpart in 2MASS and is only detected in the WISE W1 and W2 bands, making it hard to draw any conclusions based on these data. Still, its $(W1 - W2)$ color is consistent with what is seen for stars (see Figure 14 in Yan et al. 2013). Here again, the most likely source of contamination is flaring. However, the event detected by PTF had a duration $\sim 20$ days and so is highly unlikely to have been a flare. We conclude that this is a plausible candidate microlensing event.

$PTF1J172826.08+692501.1$

$PTF1J1728$ is the other candidate in the SDSS footprint. Its SDSS match, SDSS J172826.07+692501.3, has a proper motion of 1.81 mas yr$^{-1}$, consistent with its automated classification as a star. PTF1J1728 also has a counterpart in 2MASS and its SDSS/2MASS colors—$(u - g) = 1.81 \pm 0.04$, $(g - r) = 0.79 \pm 0.03$, $(r - i) = 0.35 \pm 0.03$, $(i - z) = 0.21 \pm 0.03$, $(z - J) = 0.97 \pm 0.05$, $(J - H) = 0.58 \pm 0.06$, and $(H - K) = 0.16 \pm 0.09$—are consistent with those of a K star (Covey et al. 2007). Its $(W1 - W2)$ and $(W2 - W3)$ colors place PTF1J1728 in the stellar locus in Figure 14 of Yan et al. (2013).

E. Bowsher and S. Douglas obtained two 1200 s spectra of PTF1J1728 with the MDM Observatory Modular Spectrograph (MODspec) on the Hiltner 2.4 m telescope at MDM Observa-

Figure 13. MODspec spectrum of PTF1J172826.08+692501.1, a mid-K star.

tory, Kitt Peak, Arizona, on 2012 November 14.\textsuperscript{16} MODspec was configured to provide coverage from 4500–7500 Å with $\sim 1.8$ Å sampling and a spectral resolution of $\sim 3300$. The data reduction was performed by S. Douglas using standard IRAF routines. All the spectra from this night suffered from significant noise blueward of 5000 Å and redward of 7000 Å; in Figure 13, we therefore present the spectrum over that 2000 Å range. While the spectrum is noisy, PTF1J1728 appears to be a mid-K star; its HAMMER spectral type is K3. We conclude that this is a plausible candidate microlensing event.

\subsection*{4.2. Candidates Ruled Out by Photometry and/or Imaging}

Light curves for the other eight events are shown in Figure 14 and described in detail below.

$PTF1J033545.80-041849.1$

PTF1J0335 has a counterpart in 2MASS and its $(J - H)$ and $(H - K)$ colors indicate that it is unlikely to be a star (Covey et al. 2007). Because it is only detected in the $W1$ and $W2$ bands, the WISE color does not help much: it is consistent with that of stars and of compact galaxies (see Figure 14 in Yan et al. 2013). We tentatively conclude that this is not a plausible microlensing candidate.

$PTF1J131500.09+715032.5$

PTF1J1315 has no counterpart within $10''$ in 2MASS, but is detected in all four WISE bands. The W3 image appears to have an offset nucleus compared with other filters; this could be a background source and we therefore do not use the W3 magnitude because of this possible contamination. The $(W1 - W2)$ color places the object well away from the stellar locus (see Figure 14 in Yan et al. 2013). We tentatively conclude that this is a likely extragalactic source and therefore not a plausible microlensing candidate.

$PTF1J171606.82+474423.7$

PTF1J1716 does not have a counterpart in 2MASS. Its $(W1 - W2)$ and $(W2 - W3)$ colors are consistent with this object being a QSO (see Figure 14 in Yan et al. 2013). We tentatively conclude that this is not a plausible microlensing candidate.

\textsuperscript{15} These are SDSS point-spread function (PSF) magnitudes. Typically, PSF fitting provides better estimates of isolated star magnitudes; see Stoughton et al. (2002).

\textsuperscript{16} The MDM Observatory is operated by Dartmouth College, Columbia University, Ohio State University, Ohio University, and the University of Michigan.
Figure 14. Full light curves (top) and zooms around the transient maximum (bottom) for the rejected microlensing event candidates. Flagged data points have been removed.

PTF1J174736.51+300506.9

PTF1J193330.11+451501.1

PTF1J1747 has counterparts in both 2MASS and WISE. The 2MASS colors suggest that this is not a star (Covey et al. 2007), while the WISE colors are consistent with those of a QSO (see Figure 14 in Yan et al. 2013). We tentatively conclude that this not a plausible microlensing candidate.

PTF1J1933 is detected in both 2MASS and WISE. The 2MASS colors suggest that this is not a star (Covey et al. 2007), while the WISE colors are consistent with PTF1J1933 being an elliptical galaxy (see Figure 14 in Yan et al. 2013). This interpretation is strengthened by a visual inspection of the PTF...
and WISE images, which show that the object is elongated in the northeast-southwest direction. We tentatively conclude that this is not a plausible microlensing candidate.

4.3. Candidates Lacking Sufficient Data to Evaluate Likelihood

PTF1J120642.60−192016.4

PTF1J120642.60−192016.4 has no counterpart within 10'' in 2MASS. While a counterpart is listed in the WISE data 3'' from the PTF position, a visual comparison of the coadded PTF R-band images and of the WISE images indicates that the PTF object may be blended with other objects in the WISE data or not detected at all. However, the WISE photometric flags for this nearby source suggest it is clean and unblended. The available information is insufficient to draw even tentative conclusions about the nature of this object.

PTF1J13202.91+674825.1

PTF1J13202.91+674825.1 has no counterpart in 2MASS, but is detected in the WISE W1 and W2 bands. The corresponding \((W1−W2) = −0.43 ± 0.2\) color is somewhat unusual, as most objects appear to have \((W1−W2) ≥ 0.0\), with compact galaxies being the rare exceptions (see Figure 14 in Yan et al. 2013). Here again, we cannot draw any conclusions about the nature of this object.

PTF1J17330.07+374311.9

PTF1J17330.07+374311.9 is detected in the 2MASS J and K bands (but not H). There is no object in the WISE catalog within 10'' of PTF1J1733. Although the \((J−K)\) color appears inconsistent with PTF1J1733 being a star (Covey et al. 2007), we cannot draw any firm conclusions about the nature of this object.

5. CONCLUSIONS AND FUTURE WORK

Using time-domain data from the PTF, we have developed a new method for identifying interesting transients in massive light-curve data sets and for searching for sparse-field microlensing events. We have examined the detection efficiency of recovering simulated microlensing events using a set of variability statistics adapted from Shin et al. (2009). We determined selection criteria for each statistic using Monte Carlo simulations to simulate flat light curves with Gaussian noise and by choosing the selection boundaries such that our cuts achieved a 1% FPR rate. We then simulated microlensing events in real PTF data and computed the detection efficiency for each statistic.

We found that the von Neumann ratio, \(\eta\) (or Durbin–Watson statistic; von Neumann et al. 1941; Durbin & Watson 1950), performs better than previously used statistics in recovering injected microlensing events in non-uniformly sampled data. We used \(\eta\) to develop a selection procedure for extracting microlensing event candidates from the PTF light-curve archive. Among the \(1.1 \times 10^5\) light curves with > 10 R-band observations, we first identified \(\sim 2000\) interesting candidate transients, from which we selected 11 candidate microlensing events.

A large fraction of the contaminants among the \(\sim 2000\) interesting candidates were active galactic nuclei or quasars exhibiting long-term, peaked variability. We also recovered a large number of transient events such as novae, outbursts, and flares. We have cross-referenced this list of objects with the PTF transient detection system and found that most of these objects are known sources, but we discovered at least two supernovae that the PTF pipeline had missed.

Of the 11 candidate microlensing events, we tentatively ruled out 8 by examining the available photometry and images or because they lacked such data. We labeled the 3 remaining objects as plausible microlensing events, but lacking simultaneous multi-color imaging during the events, we cannot confirm these candidates as true microlensing events.

For these three plausible events, we use a Markov Chain Monte Carlo algorithm to derive posterior probability distributions over each parameter in the point-source, point-lens microlensing model. The event durations for two of the candidates are reasonable, but the significantly longer duration of the third candidate could be a sign of a larger mass lens or larger distance.

While this number of candidate events is consistent with simple predictions, microlensing event-rate predictions away from the Galactic plane are generally not well constrained. In a forthcoming paper, we will present a detailed investigation of the all-sky microlensing event rate, generated from a model that includes realistic mass and velocity distributions (A. P. Fournier et al., in preparation).

Our algorithm identified \(\sim 2000\) transient candidates from a database of over \(10^6\) light curves, each of which we then visually inspected. Rigorously classifying and cataloging these sources was beyond of the scope of this paper, but many presented interesting forms of variability. Although it is not necessarily scalable for future surveys to look at all light curves selected by using our algorithm, these \(\sim 2000\) light curves, once carefully classified, could serve as a training set for a more sophisticated machine-learning approach (e.g., Bloom et al. 2012; Brink et al. 2013) to classify the light curves that survive our selection criteria. Approaches that combine statistical cuts such as those described in this paper and some type of machine learning will be essential for making the most of the future time-domain data such as those collected by the Large Synoptic Survey Telescope.

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This research made use of Astropy, a community-developed core Python package for astronomy (Astropy Collaboration 2013).