(Homo)polymer-mediated colloidal stability of micellar solutions

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Despite their wide range of applications, there is a remarkable lack of fundamental understanding about how micelles respond to other components in solution. The colloidal stability of micellar solutions in presence of (homo)polymers is investigated here following a theoretical bottom-up approach. A polymer-mediated micelle–micelle interaction is extracted from changes in the micelle–unimer equilibrium as a function of the inter-micelle distance. The homopolymer-mediated diblock copolymer micelle–micelle interaction is studied both for depletion and adsorption of the homopolymer. The fluffy nature of the solvophilic domain (corona) of the micelle weakens the depletion-induced destabilization. Accumulation of polymers into the corona induces bridging attraction between micelles. In fact, both depletion and adsorption phenomena are regulated by the coronal thickness relative to the size of the added polymer. Penetration of guest compounds into the coronal domain of crew-cut micelles, with a narrower yet denser corona, is less pronounced as for starlike micelles (with a more diffuse corona). Therefore, crew-cut micelles are less sensitive to the effect of added compounds, and hence more suitable for applications in multicomponent systems, such as industrial formulations or biological fluids. The trends observed for the colloidal stability of crew-cut micelles qualitatively match with our experimental observations on aqueous dispersions of polycaprolactone–polyethylene glycol (PCL–PEO) micellar suspensions with added PEO chains.

1 Introduction

Spherical micelles formed from amphiphilic block copolymers in solution have received ample interest for multiple applications, including drug delivery, coatings and are present in foodstuffs. Diblock copolymers are constituted by a solvophilic and a solvophobic block, consisting of \( n \)-solvophilic and \( m \)-solvophobic units respectively. The solvophobic blocks drive the micelle formation, as the solvophobic segments (B) tend to minimize their contact with the solvent by forming a compact, solvent-depleted core. The solvophilic blocks (A) concentrate in the well-solvated corona. From both fundamental and application perspectives, biocompatible neutral block copolymers are appealing as their self-assembly is regulated by a small set of system parameters: the length, nature, and sequence of the blocks. Even though block copolymer micelles are mainly applied in multi-component systems, there is a remarkable lack of fundamental understanding regarding how micelles respond to other components in solution, and most investigations have focused on highly concentrated micellar solutions. Significant attention has been paid to understanding how homopolymers affect the self-organization of block copolymers in bulk but little investigations have focused on block copolymer–homopolymer–solvent ternary mixtures. Here, we study how added free homopolymers affect both the self-assembly of block copolymers in solution and the colloidal interactions between the resulting self-assembled structures. The latter may be of relevance to understand conformational changes in biological systems. For instance, crowding with free polymers can tune the assembly of structures in cells, and polymer-mediated forces affect several properties of biological membranes.

Micelles made of neutral block copolymers may be considered as sterically-stabilized colloids and are qualitatively similar to polymer-grafted hard colloids, but their associative nature yields some important differences. The colloidal stability of sterically-stabilized colloids generally increases with increasing the number of polymers per unit area (grafting density) and the length of the stabilizing chains. For polymer-grafted hard colloids these parameters can be controlled independently and
are not affected by the environmental conditions. Conversely, the effective grafting density of block copolymer micelles depends on the equilibrium aggregation number of the micelles, which is controlled by the absolute and the relative length of the blocks, by their solubility and by the solution conditions (including the presence of dispersed additives). For a given lyophobic block length the aggregation number of the micelles, and hence the grafting density of the lyophilic brushes at the micelle’s core, decreases with increasing the length of the lyophilic blocks. This mutual dependence between grafting density and lyophilic block length makes it very difficult to predict whether micelles with long lyophilic blocks (star-like micelles) are more stable from a colloidal perspective than micelles with short lyophilic blocks (crew-cut micelles) in multicomponent mixtures. In fact, the presence of dispersed polymeric additives might compromise the colloidal stability of the micelles via the depletion-induced attraction or bridging flocculation mechanisms observed for hard colloids. Being able to predict such phenomena is of key importance for reliable application of block copolymer micelles in multi-component systems, such as industrial formulations and biological fluids. For instance, a micellar drug delivery system acts in the presence of a myriad of components that may alter the micellar properties and affect their colloidal stability, resulting in a reduction or suppression of their therapeutic efficiency.

The effective interaction between multi-arm star polymers is frequently used as a model for interactions between soft colloidal particles. The phase stability of dispersions containing soft colloidal particles mixed with linear polymers has been reported both theoretically and experimentally. Furthermore, micelle–micelle interactions have been compared to those between star polymers. In contrast with other theoretical approaches, we explicitly account for the associative nature of the micelles within self-consistent mean-field theory.

We use the Scheutjens–Fleer Self-Consistent Field Theory (SCFT) to investigate the colloidal stability of crew-cut and star-like micelles with a fixed lyophobic block length in the presence of dispersed (soluble) (homo)polymers. Using this theory we recently studied the solubilization of small added compounds into a block copolymer micelle and the interaction between block copolymer micelles (in the absence of additives). We showed that both phenomena are highly affected by the associative nature of the micelles. The SCFT method previously presented for the micelle–micelle interactions is extended here to account for the addition of homopolymers to the micellar suspension. We investigate how the presence of homopolymer in solution affects the micelle–unimer equilibrium, as this is directly related to the micelle free energy.

Therefore, by monitoring changes in the micelle–unimer equilibrium (i.e. the variation on the critical micelle concentration) as a function of the inter-micelle distance, it is possible to collect polymer-mediated micelle–micelle interactions. By allowing variations on the micelle’s aggregation number, we also take into account their stability with respect to dissolution. Micelle morphology transitions are not investigated, as we focus on the interaction between spherical micelles in the dilute regime. Eventual morphology transitions can however be expected at high micelle concentrations. Furthermore, homopolymer addition may change the preferred spatial organization of concentrated micelles. From the collected potentials, we calculated the second osmotic virial coefficient ($B_2$) to assess the phase stability of association colloid–polymer mixtures (ACPMs). Consider a dilute micelle suspension at a fixed diblock concentration (above the critical micelle concentration, CMC) to which guest compounds are added. If such a mixture has a $B_2$-value near or above the hard sphere limit, it is expected to remain optically transparent ($B_2 < 4$ and the micelle suspension may get turbid. In case of $B_2 < -6$, the Vliegenthart–Lekkerkerker (VL) criterion states that colloidal gas–liquid phase separation of the micellar dispersion is expected. Even though this $B_2$-value is in principle experimentally resolvable, there are many practical difficulties related to measuring $B_2$. Thus, direct visual observation of the (in)stability of the ACPM serve here as a pragmatic confirmation of theoretical predictions made. Trends found based on our theoretical model are compared with the stability of polycaprolactone–polyethylene glycol (PCL–PEO) micelles in water in the presence of added PEO chains.

Contrary to more computationally expensive approaches, SCFT computations allow us to systematically assess the effect of added homopolymers with different affinity to the corona. This allows us to study both adsorption and depletion phenomena. Whilst a lot is known about the polymer-mediate phase stability of non-associative colloids, the results presented here constitute the first systematic investigation on the colloidal stability of association colloids as far as we are aware.

2 Methods

In this section we summarise the theoretical and numerical methods used to study the diblock copolymer micelles.

2.1 SCFT for micelle–micelle interactions

We used the Scheutjens–Fleer self-consistent field theory (SCFT) to perform numerical calculations. We use the sfbox software in our numerical computations. In this method, the mean field approximation is implemented for a liquid mixture which is composed of lattice sites organised in ‘layers’ numbered as $z = 1, \ldots, N_{lat}$ similar to the Flory–Huggins theory, with $N_{lat}$ the number of lattice layers. Volume fraction profile variations between layers are allowed. On such a lattice, the Edwards equation is implemented which basically results in the discrete freely jointed chain model for the chain statistics. The incompressibility condition ($\sum_{k=1}^{N_c} \phi_k = 1$, with $N_c$ the number of components) is applied to the volume fractions $\phi(z)$ at each lattice layer, and at each lattice site $z$ a segment potential $\mu(z)$ is defined. The geometry of the lattice and the boundary conditions further define the system of interest. Micelles are modelled in a spherical lattice geometry wherein the number of lattice sites increases basically quadratically with $z$: the lattice is defined as
shells from the centre of the lattice $z = 0$ up to $z = N_{\text{latt}}$. For such a system one can write down a mean field free energy $F \equiv F(\phi, \mu, z)$, where $z$ is a Lagrange field that is coupled to the incompressibility constraint. Nearest-neighbour segment-segment interactions are captured via Flory–Huggins interaction parameters between species $i$ and $j$, $\chi_{ij}$. Note that within the Flory–Huggins approach all self-interactions are athermal: $\chi_{ii} = 0$. We choose the self-interactions as zero, which sets the reference for the other interactions present. Extremisation of the mean-field free energy leads to the self-consistent field relation:

$$\phi_i(z_k) \leftrightarrow u_i(\phi_k),$$

which is numerically solved. Mirror boundary conditions are set at $z = N_{\text{latt}}$. The lattice layer at $z = 0$ corresponds to the centre of the spherical micelle. Lengths are expressed in terms of lattice units [l.u.]. As we focus on conditions where spherical micelles are preferred over other self-assembled structures, a spherical lattice is used in our calculations. Due to the mirror conditions imposed, a micelle is effectively formed in the presence of $K$ surrounding ones. The distance between the centres of two nearest neighbour micelles $r$ defines the characteristic length scale involved in the pair potential calculation. For a spherical lattice, $K \approx 12$ and $r = 2N_{\text{latt}}$.20

The SCFT approach accurately resolves the equilibrium properties of the system of interest. From the free energy, one can derive other thermodynamic functions such as the grand potential $\Omega$, which is a central quantity in the small system thermodynamics approach.46 Via $\Omega$, the conditions under which the diblock copolymers form self-assembled morphologies can be resolved. To find the equilibrium configuration, we compute the grand potential $\Omega$ of the system for a specific diblock copolymer as a function of the aggregation number $g_p$, which is the number of diblocks per micelle. This grand potential relates to the inhomogeneities in the system (i.e., for any homogeneous bulk phase such as a pure solvent or a polymer solution $\Omega = 0$). As diblock copolymers are added to the solution, $\Omega$ increases due to the unfavourable contacts present between solvent molecules and solvophobic blocks. The appearance of the first thermodynamically stable micelle is marked by a maximum in $\Omega$. If a micelle can form, $\Omega$ decreases with $g_p$, and at a given diblock concentration the condition $\Omega_{g_p = 0} = 0$ is met (with $2\Omega_c g_p < 0$). At this condition, the most probable micelle (ignoring translational entropy effects) is found. Following the thermodynamics of micelle formation, the micelle is in equilibrium with free block copolymers in the bulk. Hence, the chemical potential $\mu_p$ of one copolymer in the micelle $\mu_{p, \text{micelle}}$ is equal to that in the bulk $\mu_{p, \text{bulk}}$:

$$\mu_{p, \text{bulk}} = \mu_{p, \text{micelle}} \equiv \mu_p \approx \text{const} + T \ln \phi_p \text{bulk},$$

with $\phi_p$ being the bulk polymer segment volume fraction, $k_B$ the Boltzmann’s constant, and $T$ the absolute temperature. The last equality holds whenever $\phi_p$ is small. Once an equilibrium micelle is found, its equilibrium characteristics can be extracted directly from SCFT. The work $\omega$ required to dissociate all polymers from the self-assembled structure (equivalently, the energy gain of the diblocks upon micellization) at a certain intermicelle distance $r$ follows as:46

$$\omega(r) = g_s(r)\mu_p(r) + g_r(r)\mu_r(r) + g_a(r)\mu_a(r),$$

where $g_s$ and $g_a$ are the excess number of solvent and homopolymer; $\mu_s$ and $\mu_a$ are the corresponding chemical potentials. It must be noted that the sfbox software provides the chemical potential (accounting for activity coefficients) of all compounds considered, and this is the one we use in our computations. This $\omega(r)$ might be interpreted as a chemical potential for the micelle as a whole for specified distance between two micelles $r$ (i.e., the Gibbs free energy per micelle). These SCFT-provided equilibrium quantities enable us to estimate the interaction $W$ between micelles as:20,47,48

$$W(r) = \frac{2}{k_B} [\omega(r) - \omega(r = \infty)].$$

Typically, we normalise this micelle–micelle interaction to the thermal energy, i.e., we present $\beta W(r)$, where $\beta \equiv 1/(k_BT)$. Note here the approximations made in the derivation of the above-mentioned interaction. The imposed condition that $\Omega = 0$ at each inter-micelle distance implies that always the most stable equilibrium micelle is formed; in reality the unimer-solvent exchange may be slower than average time of collision between micelles.49–51 We exploit the equilibrium properties computed from SCFT as a route for calculating the micelle–micelle interactions which are fully adaptative. Alternatives to calculate micelle–micelle interactions for ‘frozen’ micelles may differ from the one here presented.52 Our approach does not imply any pre-set interaction between the coronas, but rather evaluates how the change of the surroundings of the micelle affects the equilibrium self-assembly properties ($\Omega = 0$ at each intermicelle distance). We extract interactions between the micelles, which originate naturally from the equilibrium properties of micelles formed at a given $r$. For small enough values of $r$ the coronas start to overlap, affecting the equilibrium micelle formation conditions and hence the free energy of micelle formation.20

From the micelle–micelle interactions, the second (osmotic) virial coefficient ($B_2$) can be extracted to assess the stability of the colloidal suspension.34,35 For any form of the pair interaction $W(r)$, the second virial coefficient follows as:

$$\frac{B_2}{\nu_c} = 12 \int_{r=0}^{\infty} \rho (1 - \exp[-\beta W(r)]) dr,$$

where $\nu_c$ is the colloidal particle volume, taken here as the undistorted micelle hydrodynamic volume, $\nu_c \equiv (4\pi/3)[R_0^3]$, and with $r \equiv r/(2R_0)$ the normalised inter-micelle distance with $R_0$ the undistorted (homopolymer-free) micelle size. As the micelle–micelle interactions are not resolvable for $\rho \ll 1$, interpolation of the SCFT-generated results at the smallest resolved $\rho$ is

\[ 2.2 \text{ System parameters} \]

We followed the approach outlined in the previous section to collect (homopolymer-mediated micelle–micelle interactions. When considering diblock copolymer micelles in the presence
of polymers in a common solvent, the key variables are those reported in Fig. 1. Specifically, these variables are: (i) the different segment–segment and segment–solvent interactions; (ii) the equilibrium micelle properties, and (iii) the relative size of homopolymer to micelle and its bulk concentration. Contrary to more computationally expensive methods, in the SCFT approach followed one can easily scan this parameter space.

Table 1 System parameters chosen in this study: number of solvophobic (m), solvophilic (n), and guest polymer segment (N) repeating units, and Flory–Huggins interaction parameters. A and B refer to a solvophilic and solvophobic segment, respectively; G denotes a guest homopolymer block, and W the solvent. Further specified are the hydrodynamic micelle radius \( R_m \), the corona thickness \( T \), the core radius \( R_c \), and the radius of gyration of the homopolymer \( R_g \). We highlight the parameter \( \chi_{AG} \) which determines whether homopolymers are depleted or adsorbed.

| m | n | N | \( \zeta_{BW} \) | \( \zeta_{AW} \equiv \chi_{GW} \) | \( \zeta_{AB} \equiv \chi_{GB} \) | \( \zeta_{AG} \) |
|---|---|---|---|---|---|---|
| 24 | 45, 450 | Var | 2 | 0.4 | 1 | var |

where the radius of gyration of the free homopolymer composed of \( N \) segments in solution is approximated as:

\[
R_g = 0.309 b N^{1/2} \left[ 1 + \sqrt{1 + 6.5 N^{1/2} (1 - z_{GW})} \right]^{0.52},
\]

where \( b \) is the monomer size which equals the size of a lattice site and \( R_m \) is the hydrodynamic radius of an isolated micelle in absence of homopolymer (for details on the calculation of \( R_m \), see for instance \(^{56}\) and references therein). The experimentally-resolvable value for \( R_m \) qualitatively agrees with theoretical predictions for diblock copolymer micelle systems. \(^{57}\) Though approximate, eqn (6) captures the SCFT-predicted trends for the radius of gyration of an isolated guest homopolymer chain. The \( q \)-value is commonly used to quantify depletion phenomena. \(^{56}\) Provided \( R_m \) is known, the size of the homopolymer can be obtained via eqn (5) and (6) for a certain (imposed) \( q \)-value. We conducted our computations at fixed homopolymer bulk concentration \( \phi_G^{bulk} \). The homopolymer overlap concentration is defined as:

\[
\phi_G^* = \frac{N b^3}{v_G},
\]

with

\[
v_G = \frac{4 \pi}{3} R_g^3
\]

the estimated volume occupied by a (guest) homopolymer coil in the bulk solution. The solvent quality of the guest (G) polymer is considered to be equal to that of the solvophobic block segments \( (\chi_{GW} \equiv \chi_{AW} = 0.4) \), and the solvophobic segment–homopolymer interaction is considered to be equal to the one between A and B segments \( (\chi_{GB} \equiv \chi_{AB} = 1) \). The effective affinity of the guest compound to the corona of the micelle is varied through \( \chi_{AG} \), where \( \chi_{AG} = 0 \) corresponds to athermal (only excluded volume) corona–homopolymer interactions.

We identify whether the homopolymer is adsorbed onto or depleted from the micelle in terms of the adsorption thickness \( \delta \), defined here from the discrete SCFT density profile \( \rho_G(z) \) as:

\[
\delta = \frac{N_{lat}}{\rho_G^{bulk}} - 1,
\]

where \( z_0 \) is the considered offset layer, and \( z = \{1, 2, \ldots, N_{lat}\} \), with \( N_{lat} \) the lattice size considered. This offset layer was chosen as the closest layer to \( R_m \); \( z_0 \approx R_m \).

2.3 Experimental methods

Block copolymers PCL12PEO45 have been synthesized and purified, and the micelle dispersions have been prepared as in previous works. \(^{55}\) The undistorted hydrodynamic radius of the resulting micelles (\( R_m^{exp} = 9 \) nm) was measured using dynamic light scattering (DLS). DLS experiments were performed by means of an ALV CGS-3 equipped with a 532 nm green laser. The polymers used as depletants, namely PEO45, PEO136 and PEO227, were purchased from Sigma-Aldrich and have been used as received. The \( R_g \) value of these copolymers (\( R_g = 1.4, 2.6 \) and 3.4 nm respectively)
have been calculated using eqn (6) assuming \( b = 0.4 \) nm.\(^{55}\)

The overlap concentrations of these polymers have been estimated upon applying eqn (7), while the polymer volume fraction in solution have been calculated dividing the polymer mass concentration by the polymer density \( \rho = 1.125 \) g \( \times \) cm\(^{-3}\).\(^{58}\)

3 Results and discussion

We first discuss the equilibrium properties of micelles and the concentration distribution of diluted homopolymers as a function of the homopolymer-corona effective affinity. Subsequently, homopolymer concentration effects on the micelle equilibrium are studied for different guest polymer–micelle combinations (crew cut, starlike, depleted, adsorbed). Additionally, the stability of association colloid–polymer mixtures (ACPMs) is investigated, and results are discussed in terms of the second virial coefficient \( B \).

Representative homopolymer-mediated micelle–micelle interactions are rationalised in Appendix A.

Table 2

| Unimer      | \( g_p \) | \( \phi_{p}^{\text{bulk}} \) | \( \phi_{p}^{\text{bulk}} \approx \) CMC | \( \phi_{A}^{\text{max}} \) | \( R_{0} \) | \( R_{c} \) | \( T \) |
|-------------|---------|-----------------|----------------|----------------|--------|--------|------|
| B\(_{24}A_{45}\) | 134     | \( 3.6 \times 10^{-8} \) | 0.31           | 19.5           | 11     | 8.5    |
| B\(_{24}A_{450}\) | 37      | \( 1.3 \times 10^{-5} \) | 0.20           | 48.3           | 8      | 40.3   |

Fig. 2  (a and b) Micelle-forming diblock segment radial volume fraction profiles from the centre of a micelle, computed using SCFT in a spherical lattice considering a crew-cut \([B_{24}A_{45}, (a)] \) and a starlike \([B_{24}A_{450}, (b) \) micelle. Core (orange) and corona (purple) regions are indicated; dashed lines indicate the core radius \( (R_{c}, \text{grey}) \) and the calculated hydrodynamic radius \( (R_{0}, \text{black}) \). Insets as main plots, but in a linear scale. (c and d) Homopolymer radial volume fraction profiles relative to the bulk concentration. All results refer to calculations for a dilute homopolymer solution (\( \phi_{p}^{\text{bulk}}/\phi_{p}^{*} = 10^{-4} \)) with relative size \( q \equiv R_{d}/R_{0} = 0.2 \). In the insets, the adsorption thickness \( \delta \) as a function of the corona-homopolymer effective affinity \( \chi_{AC} \) is plotted. The \( \chi_{AC} \)-values used in the main plot are indicated with discs: \( (0.25, 0, -0.25, -0.5) \).

3.1 Homopolymer depletion and adsorption in spherical micelles

Some SCFT-computed characteristics of isolated crew-cut and starlike micelles are presented in Table 2. The different architectures of the unimers leads to distinct properties of the micelle, reflected in the aggregation number \( g_p \), critical micelle concentration (CMC), and sharpness of the corona (expressed through the maximum concentration of solvophilic blocks \( \phi_{A}^{\text{max}} \)). Due to the (much) lower \( g_p \)-value but larger \( R_{0} \)-value of the starlike micelle compared to the crew-cut one, the available surface area per diblock of a starlike micelle is significantly larger than for a crew-cut one.\(^{20}\) Hence, the peripheral region of the starlike micelle is more diffuse than for the crew-cut one. The CMC is controlled at first order by the solvophobic block length.\(^{59}\) However, due to the larger solvophilic to solvophobic block size ratio of the starlike micelle, its CMC (expressed here via the diblock bulk volume fraction \( \phi_{p}^{\text{bulk}} \)) is about 500 times larger. Consequently, the unimer-micelle equilibrium upon addition of guest homopolymer is expected to be more affected for a starlike micelle than for a crewcut one.

Equilibrium radial volume fraction profiles are shown in Fig. 2(a) and (b) as a function of the distance from the centre of the micelle \( z \). The maximum concentration of solvophilic blocks \( \phi_{A}^{\text{max}} \) roughly coincides with the position of the core–corona interface, used here as estimated core radius \( (R_{c}, \text{grey}) \).

The corona thickness (defined as \( T = R_{0}^{\text{c}} - R_{c} \)) is obviously larger for the starlike micelle, which has a smaller \( R_{c} \) due to the much lower value of \( g_p \). The lower \( \phi_{A}^{\text{max}} \)-value also indicates that the
outer region of the starlike micelle is overall less dense than for the crew-cut assembly.

Not only the relative size of the homopolymer and its concentration modulate the effective micelle–micelle interactions, but also the affinity between the homopolymer and the outer micelle region (i.e., the corona). Homopolymers in solution are either depleted from or adsorbed to the corona domain, depending on the affinity between the corona blocks and the homopolymer. In Fig. 2(c) and (d), the normalised homopolymer volume fraction ($\phi_G$) plotted as a function of $z$ at fixed $\phi_{G\text{bulk}} = 10^{-4}$. For $\Delta AG < 0$ homopolymers are depleted ($\phi_G < \phi_{G\text{bulk}}$) from the micelle, with $\phi_G(z = R_c) \approx 0$. Due to the entropic penalty of homopolymers being near or within the micelle, $\phi_G$ decreases with respect to $\phi_{G\text{bulk}}$ if $\Delta AG$ attains a sufficiently large (repulsive) value.

For $\Delta AG = -0.25$ adsorption occurs and $\phi_G(z \lesssim R_h)$ is larger than for $\Delta AG = 0.25$ or $\Delta AG = 0$, see Fig. 2(c) and (d). For the crew-cut micelle the homopolymer practically does not adsorb at $z > R_h$ for $\Delta AG = -0.25$, and is still partially depleted from $R_c$ (note there is a finite homopolymer concentration at $R_c$). For the starlike micelle, $\phi_G$ reaches a pronounced maximum value above $\phi_{G\text{bulk}}$ within the corona; yet it is also partially depleted close to the core ($z \to R_c$). This suggests that the degree of penetration of the added polymer into the coronal domains modulates the athermal interactions of ACPMs. For $\Delta AG = -0.5$, $\phi_G$ is always greater than $\phi_{G\text{bulk}}$ for $z$-values within the corona: homopolymer adsorption to the corona occurs. The adsorption thickness $\delta$ (see Methods) indicates whether depletion ($\delta < 0$) or adsorption ($\delta > 0$) takes place. The transition from homopolymer depletion to adsorption is observed in the insets of Fig. 2(c) and (d) in terms of $\delta$ as a function of $\Delta AG$. Near $\Delta AG = -0.25$, the sign of $\delta$ switches from negative (depletion) to positive (adsorption). The thickness of the depletion layer $\delta$ increases with increasing $\Delta AG$ until it reaches a plateau, in accordance with what is expected for depletion from a hard surface. The dramatic increase in $\delta$ upon homopolymer adsorption upon lowering $\Delta AG$ is also in line with observations of homopolymer adsorption at a hard surface.\textsuperscript{21}

### 3.2 Add tion of homopolymer modulates the micelle–unimer equilibrium

The homopolymer concentration considered in the previous section was in the dilute regime to study adherence to the micelles. Here, the focus is on elevated homopolymer concentrations at which the micelle–unimer equilibrium is affected. Firstly, we focus on cases where depletion of the homopolymer is observed in Fig. 2. Particularly, we study the effect of homopolymer concentration ($\phi_{G\text{bulk}}$) on the equilibrium local density profiles near and within an isolated micelle. In Fig. 3 the influence of homopolymer depletion on the aggregation number, expressed in terms of $\Delta G_p = G_p(\phi_{G\text{bulk}}) - G_p(\phi_G = 0)$ is shown. It follows that the aggregation number of both kinds of micelles increases with increasing $\phi_{G\text{bulk}}$. This agrees with previously reported experimental observations.\textsuperscript{3} The increase in $G_p$ is weaker when the homopolymer size is larger (i.e., increasing $q$). For large homopolymers it is more difficult to penetrate the corona. Interestingly, the micelle size is hardly affected by these changes in $G_p$. In fact, upon averaging over all considered $q$-values and $\phi_{G\text{bulk}}$ concentrations in Fig. 3, we find for the crew cut micelle ($R_h = 19.8 \pm 0.2$ [l.u.]) and for the starlike micelle ($R_h = 48.0 \pm 0.9$ [l.u.]), these values are fairly close to the depletant-free, undistorted micelle sizes presented (see Table 2). The addition of homopolymer to the bulk reduces the effective volume available for the free block copolymers, as they cannot access the portion of the solvent within the solvated (homopolymer) coils. Consequently, the micelle–unimer equilibria shifts towards the micelle, thus increasing $G_p$. This is confirmed by the fact that for $q = 0.2$ and $\Delta AG = 0.5$, $G_p$ is larger than for $\Delta AG = 0$ at the same $\phi_{G\text{bulk}}$. The steeper increase of $G_p$ for the starlike micelle follows from its (much) higher $\phi_{G\text{bulk}}$ (see Table 2).

Next, we study the effect of corona-adsorbing homopolymers on the equilibrium micelle properties at fixed (homopolymer)-to-micelle size ratio $q$. In Fig. 4, the variation on $G_p$ due to polymers with an enthalpic preference for the corona is reported ($\Delta AG < 0$), and compared to guest polymers with athermal interaction with the corona ($\Delta AG = 0$). For isolated micelles and low guest polymer concentrations, adsorption to the corona of the starlike micelle is much higher than to the crew-cut one (detailed profile in Appendix B). Contrary to the depletion case, the micelle–unimer equilibria shifts towards the unimer side due to favourable diblock–homopolymer interactions in the bulk (i.e., the addition of (homopolymers effectively increases the solvent quality). For a sufficiently strong solvophilic block–homopolymer affinity, homopolymers adsorbed at the core–corona interface
3.3 On the stability of ACPMs: crew-cut homopolymers over the micelles.

In this last Results section, the colloidal stability of association colloidal–polymer mixtures (ACPMs) is assessed in terms of the entropic penalty associated with the interpenetration of the homopolymers in the corona. This leads to the observed increase of $g_p$ at very low $\phi_{G}^{\text{bulk}}$. Saturation of the corona with homopolymers then leads to a decrease of $g_p$ at higher $\phi_{G}$, homopolymer-diblock contacts in the bulk become, again, more favourable than in the saturated micelle. The curves for $\gamma_{AG} = -0.45$ and $\gamma_{AG} = -0.55$ for the starlike micelle corroborate this explanation. The same effect on $g_p$ could be observed for stronger attractions ($\gamma_{AG} \approx -0.7$) of the homopolymer with the corona domain of the crew-cut micelle. From our theoretical investigations [see also32 for encapsulation of small ($q \ll 0.1$) guest compounds], it is clear that the changes on $g_p$ and $R_o$ can be used to experimentally assess the distribution of adsorbing homopolymers over the micelles.

3.3 On the stability of ACPMs: crew-cut vs. star-like

In this last Results section, the colloidal stability of association colloid–polymer mixtures (ACPMs) is assessed in terms of the second osmotic virial coefficient $B_2$, calculated from the polymer-mediated micelle–micelle interactions (see Appendix A).

We consider the colloidal particle volume as the one of an isolated micelle and without any added homopolymers, $v_o = v_h = (4\pi/3)(R_o^3)$. In Fig. 5, $B_2^* \equiv B_2/v_o$ is shown for $q = 0.2$ as a function of the homopolymer concentration $\phi_{G}^{\text{bulk}}/\phi_{G}^{*}$ at fixed homopolymer-to-micelle size $q = 0.2$. These $B_2^*$-values follow from interactions as those presented in Fig. 8–10. We focus first on homopolymers which only interact via excluded volume with the coronal domain, $\gamma_{AG} = 0$. Both for crew-cut and starlike micelles, $B_2$ decreases only weakly upon addition of homopolymer: the depletion zone spans through the coronal domains and hardly on the outside of the micelles, rendering depletion effects weak. The colloidal stability decreases dramatically from $\phi_{G}^{\text{bulk}}/\phi_{G}^{*} \approx 0.1$ when depletion effects arise via a corona-homopolymer effective affinity with an enthalpic repulsion beyond the excluded volume ($\gamma_{AG} = 0.25$). Hence, it is expected that a suspension of micelles gets unstable at high homopolymer concentrations. Due to the wider coronal region, depletion-induced destabilisation of a starlike micelle-depletant mixture occurs at slightly higher homopolymer bulk concentration. For starlike micelles, the depletion effects are weaker due to the deeper penetration of homopolymer into the corona.

Adding weakly-adsorbing homopolymers ($\gamma_{AG} = -0.25$) to a crew-cut micelle suspension leads to a mostly $\phi_{G}^{\text{bulk}}$-independent micelle–micelle interaction. For stronger homopolymer-solvophilic block attraction ($\gamma_{AG} = -0.5$), bridging attraction and restabilisation is observed in terms of $B_2$. The trends observed considering (weakly) adsorbing homopolymers show that starlike micelles destabilize more easily than the crew-cut analogues. For adsorbing polymers at high $\phi_{G}$, starlike micelles are more easily destabilized.

In micelle applications (such as drug-delivery systems), components with different affinities for the corona blocks may be present. In virtue of their shorter relative hydrophilic block length, we expect that crew-cut micelles are overall more stable in multicomponent systems due to, in essence, a denser and narrower coronal region.

To verify the reliability of our approach, we compared the SCFT predictions with experimental observations on crew-cut micelles. The set of interaction parameters used in this study is suitable to describe polycaprolactone–polyethylene glycol (PCL–PEO) diblock copolymer micelles55 in water. An aqueous suspension of such spherical micelles was prepared (the block copolymer composition was CL12EO45, see Methods for details), and mixed with free PEO homopolymers of different molar masses at different concentrations. A CL monomer is roughly twice as large as an EO monomer,55 therefore, CL12EO45 may be mapped onto our B24A45 model crew-cut micelle. In Fig. 6(a) we show photographs of mixtures of micelles (diblock copolymer concentration is 5 mg ml$^{-1}$) mixed together pure PEO at fixed concentrations. Due to the undistorted micelle volume for $q = R_f/R_o = 0.2$ for crew-cut (a) and starlike (b). The effective affinity between the homopolymer and the coronal domain is indicated.
concentration $\varphi/\varphi^*$, where $\varphi$ denotes experimentally-resolved PEO concentrations for various (weight-averaged) molar masses: I, $M_w = 2$ kDa; II, $M_w = 6$ kDa; and III, $M_w = 10$ kDa. Photographs IV, II, and VI refer to a single type of PEO ($M_w = 6$ kDa, corresponding to $N = 136$) for various PEO concentrations. In Fig. 6(b) and (c) we plot the SCFT-predicted $B_2$ values as a function of the relative polymer size (b) and polymer concentration (c). As experimentally observed, for theoretically-calculated $B_2^* \lesssim -6$ gets unstable. Sample II is stable but clearly more turbid than Samples I and IV. This can be explained by a significant free PEO-induced micelle–micelle attraction ($B_2^* \lesssim 0$), although the attractions not yet sufficiently strong to induce demixing.

4 Conclusions

In this paper, homopolymer-mediated micelle–micelle interactions were studied using numerical lattice computations based on the Scheutjens–Fleer self-consistent field theory, which explicitly considers the associative nature of the micelles. We quantified how the addition of soluble homopolymer in bulk shifts the unimer-micelle equilibria and study the effect of different affinities between the homopolymer and the outer coronal blocks on the structure of the micelle. The resulting changes of the bulk unimer concentration determine the micelle properties, particularly the aggregation number ($Q_0$). In line with previous experimental observations, homopolymer depletion leads to an increase of the aggregation number which can be rationalised in terms of the micelle–unimer equilibria. For added homopolymers which are attracted to the solvophilic blocks, weak adsorption leads to a decrease of the aggregation number with increasing homopolymer bulk concentrations. Above a certain affinity threshold, the aggregation number first increases and then decreases with increasing homopolymer bulk concentration.

In case of non-adsorbing homopolymers, the diffuse micellar outer region leads to small effective depletion layers because they penetrate into the coronas. Despite the broader depletion profile as compared to near hard spheres, depletion effects are weaker as the overlap of depletion layers is screened by the presence of the fluffy corona. Even at intermicelle distances in the order of their (undistorted) diameter, full homopolymer depletion may not be observed. Not surprisingly, an added enthalpic repulsion between the corona-forming blocks and the guest homopolymer enhances depletion effects. A strong enough guest polymer affinity to the corona leads to an almost classical polymer-mediated interaction between crew-cut micelles: bridging flocculation at low concentrations, and reestablishment upon saturation of the corona. Remarkably, weakly-adsorbing polymers may not affect the stability of the micellar suspension if the enthalpic and entropic effects of homopolymers in the coronal domain are balanced. For starlike micelles, bridging within the coronal domains leads to attractions which only increases with increasing polymer bulk concentration (up to the near-overlap concentrations studied). The packing of the homopolymer in the corona determines whether the micelle–micelle steric repulsion vanishes at high enough homopolymer concentrations. If the corona thickness is of the order of the added homopolymer diameter, a repulsive contribution to the micelle–micelle interaction is expected to be present.

From the second virial coefficient ($B_2$) we observe that both crew-cut and starlike micelles are destabilized at high enough non-adsorbing homopolymer concentration due to a (weak) depletion attraction. In case of added adsorbing homopolymer, the $B_2$-value of the crew-cut micelle–homopolymer mixture is less sensitive than for the starlike case. The trends predicted by our SCFT computations for the crew-cut micelles are qualitatively confirmed experimentally using biocompatible PCL–PEO diblock copolymer micelles in water and added free PEO homopolymer. We deduce from our investigation that a narrower coronal domain makes spherical micelles more suitable for applications, such as drug-delivery systems, where multiple macromolecular components are present. We encourage experimentalists to compare their results to our SCFT predictions. Requests for the SFbox program can be submitted to F. A. M. Leermakers, Wageningen University.

Conflicts of interest

There are no conflicts to declare.

Appendix

A Micelle–micelle interactions

In this Appendix some example pair-potentials calculated are presented and discussed.

A.1 Depletion in ACPMs

Homopolymer volume fraction distributions for selected $Q_0^{\text{bulk}}$ values are shown in Fig. 7. The observed partial penetration of homopolymers in the coronal domain has been previously reported, and such interpenetration also occurs between polymer brushes and free homopolymer, and in polymer-grafted spheres in
a polymeric matrix. With increasing homopolymer bulk concentration, $\phi_0$ decreases due to the increasing osmotic pressure that bulk homopolymers exert onto those in the vicinity or within the diffuse micelle’s peripheral region. This effect is well-known for non-adsorbing polymers near a hard surface. As depletants penetrate through the coronal region, this compression of the depletion layer is weaker for a micelle than for a hard colloidal surface. As can be observed, the shape of the depletion profile resembles that of non-adsorbing homopolymers in Θ-solvent around a hard sphere [\textsuperscript{56} \textsuperscript{56} \textsuperscript{56}] $[\tanh^{2}(z - z_0)/|\phi_0|]$. However, in this case the depletion density profile extents in between the limits of a ‘classical’ depletion profile from hard spheres with radii $R_h$ and $R_c$ (dashed vertical lines in Fig. 7). A broader coronal thickness leads to a wider depletion profile for the star-like micelles.

In Fig. 8 the micelle–micelle interactions in presence of depleted homopolymers are presented. At low depletant concentrations ($\phi_{\text{bulk}}/\phi_{\text{G}*} = 0.01$), the micelle–micelle interactions can be described as a hard-core Yukawa.\textsuperscript{29} At higher $\phi_{\text{bulk}}$ pure excluded volume interactions of the homopolymer with the coronal blocks ($\chi_{\text{AG}} = 0$) induce a shallow minimum in the micelle–micelle interaction between crew-cut micelles. This minimum is due to the homopolymer-induced depletion attraction between micelles. The position of this minimum shifts towards $r = 2R_h$ with increasing $\phi_{\text{bulk}}$ due to the compression of the depletion layer [inset of Fig. 8(a)]. For the starlike micelle considered, $\chi_{\text{AG}} = 0$ is insufficiently repulsive to induce an attractive minimum in the interaction potential between the micelles [inset of Fig. 8(b)]; the micelle–micelle interaction is only repulsive. This weakening of the steric repulsion between micelles upon adding free non-adsorbing homopolymers has also been reported for the interaction between star polymers.\textsuperscript{25} This micelle–micelle repulsion significantly weakens in $r < 2R_h$ with increasing $\phi_{\text{bulk}}$. These effects are further rationalised in Appendix A.3. For $\chi_{\text{AG}} = 0.25$, a minimum in the homopolymer-mediated micelle–micelle interactions is present for the two kinds of micelles as a result of more repulsive hydrophilic block-homopolymer interactions, which effectivly shifts the depletion zone towards the outer micelle region: there is not only an entropic, but also an enthalpic penalty whenever depletants penetrate into the coronal domain. The trends observed in the micelle–micelle interactions in case of homopolymer depletion match with expectations based upon the interactions between soft colloids;\textsuperscript{35,27} the interaction weakens as the outer coronas get more fluffy.

Experimentally, depletion effects decrease the effective (hard-sphere equivalent) colloidal size of the micelle, which may relate to the lack of a repulsive contribution to the micelle–micelle interaction observed for the starlike micelle at high enough homopolymer concentrations.\textsuperscript{9} We note here that whereas $|\phi_0|$ decreases with $\phi_{\text{G}*}$, this decrease is not enough (in hard colloidal suspensions) to re-stabilize the depletion attraction, whose strength increases with $\phi_{\text{G}*}$. The overlap of depletion zones when micelles get closer does not lead to full depletion of the guest homopolymer, even if an added enthalpic penalty is considered (profile details in Appendix B). From the trends of the depletion profiles and of the micelle–micelle interactions, we conclude that the depletion attraction is weaker in micellar suspensions than in hard colloidal systems due to the inherent steric repulsion and the penetration of the depletants into the micellar domain. Insights into micelle–micelle interactions may be of relevance for further understanding the effects of depletion phenomena in systems where micelles are present, such as drug-delivery\textsuperscript{4} or foodstuffs.\textsuperscript{6}

A.2 Coronal physisorption in ACPMs

In Fig. 9, example micelle–micelle interactions mediated by corona-adsorbing homopolymers are shown. For crew cut-micelles, a slight preference for the coronal blocks ($\chi_{\text{AG}} = -0.25$) hardly affects the pair interactions upon increasing $\phi_{\text{G}*}$ even close to $\phi_{\text{G}*}$, the micelle–micelle interaction mostly remains unaffected. For a stronger homopolymer–coronal affinity ($\chi_{\text{AG}} = -0.5$), a shallow attraction at low $\phi_{\text{G}*}$ appears, which then weakens with increasing $\phi_{\text{G}*}$ (inset of Fig. 9). This can be explained by a bridging attraction mechanism:\textsuperscript{21} at low concentration homopolymers simultaneously adsorb onto the coronas of different micelles, which leads to attraction between them. This trend of the bridging attraction between micelles with increasing $\phi_{\text{bulk}}$ is similar to that observed between hard colloids.\textsuperscript{21} With increasing $\phi_{\text{bulk}}$, the coronal domains may get saturated with homopolymer, leading to a restabilisation of the micelle suspension. The homopolymer-mediated micelle–micelle bridging attraction results from the intricate combination of homopolymer configuration changes (loop-to-bridge) and micelle–unimer equilibria. Perhaps, fewer loops transform intro bridges as compared to the attraction between hard spheres due to the fluffy and diffuse nature of the interface. This leads to a weaker bridging attraction between micelles as between hard spheres.

As for the depletion cases, the effect of adsorbing polymer is more convoluted for starlike micelles due to their broader corona. For the $g$-value considered ($g = 0.2$), the relative volume...
of the (undistorted) homopolymer per coronal block is about four times larger for the starlike micelle than for the crew-cut one (see Appendix B). Note that at fixed $q$ and $\chi_{AG}$, adsorption is much higher for the starlike micelle than for the crew-cut one (see profiles in Appendix B). Hence, bridging effects are strong for starlike micelles as they get closer. The large and fluffy corona prevents saturation of the peripheral ‘colloidal domain’, at least within the considered $\phi_G$ values. Thus, contrary to the crew-cut micelle, re-stabilisation of the bridging flocculation is not observed in the micelle–micelle interactions even at high $\phi_G$. The steric micelle–micelle repulsion gets screened due to the presence of adsorbing homopolymer, leading to a transition from repulsive to attractive micelle–micelle interaction. The larger coronal domain may favour the loop-to-bridge transition, which becomes dominant over the steric repulsion. In the next section, the relevance of the relative size of the added homopolymer to the coronal thickness is addressed: penetration of homopolymer is rationalised not in terms of $q \equiv R_g/R_h^*$, but in terms of $R_g/T$.

### A.3 Corona thickness and colloidal stability

It is clear from the computed micelle–micelle interactions that a high degree of interpenetration of either adsorbing or depleted compounds into the coronal domain leads to destabilisation of the micelle suspension with increasing the guest homopolymer concentration $\phi_G^{\text{bulk}}$. In block copolymer/homopolymer blends, the degree of homopolymer penetration in the corona is related to its length relative to the corona-forming block length.\textsuperscript{13} For the relative size $q = 0.2$, the starlike micelle–micelle steric repulsion practically vanishes at $\phi_G^{\text{bulk}}/\phi_G^{*} = 0.75$ [see Fig. 8(b)]. Within the model here considered, the strongest repulsive contribution to the (homopolymer-free) micelle–micelle interaction arises from the expel of diblocks.\textsuperscript{20} Independently of the value of $\chi_{AG}$, the presence of homopolymers in the corona may screen this strongly-repulsive core compression. For the crew-cut micelle considered, $q \approx 0.2$ corresponds to the situation where the diameter of the added homopolymer roughly equals the coronal thickness ($2R_h = T$). For a starlike micelle, this situation is retained for $q \approx 0.4$.

We present in Fig. 10 the homopolymer-mediated starlike micelle–micelle interaction for $q = 0.4$ and $\chi_{AG} = 0$. This micelle–micelle interactions are similar to those between crew-cut micelles at $q = 0.2$ (for which $R_g = T/2$); for larger $q$, fewer polymer chains fit into the corona, and a repulsive contribution to the homopolymer-mediated micelle–micelle interaction remains. The much higher $\phi_G^{\text{bulk}}$ value for the starlike micelle renders all guest homopolymer effects on the micelle equilibria stronger due to the lower energy required to remove a diblock from the starlike micelle as compared to the crew-cut one. This leads to a clear decrease of the repulsive contribution to the micelle–micelle interaction, which decreases from $W(r = 2R_h^*) \approx 10k_BT$ in absence of homopolymer to $W(r = 2R_h^*) \approx 5k_BT$ at $\phi_G^{\text{bulk}}/\phi_G^{*} = 0.75$. It follows from this short section that it is the ratio of the corona thickness to the diameter of the added homopolymer which determines whether a repulsive contribution to the micelle–micelle interaction is present upon addition of homopolymer. Therefore, the ratio $R_g/T$ might be of relevance in the design of controlled experiments. In fact, it has been experimentally shown that this ratio controls the homopolymer-induced aggregation of vesicles in water upon homopolymer addition.\textsuperscript{55}

### B Packing arguments and concentration profiles

The relative volume of a corona block in the micelle per undistorted homopolymer volume $Q$ can be derived from geometrical arguments:

\[
Q = \frac{8\pi R_g^3}{(R_h^{\text{max}})^3 - (R_h^*)^3}
\]  

(10)

For $q = 0.2$, we get for the crew-cut micelle $Q = 1.25$ and for the starlike one $Q = 0.3$. We present in Fig. 11 the homopolymer radial volume fraction profiles upon varying the intermicelle-
distance. Homopolymer depletion profiles for isolated \((r \gg 2R_h^0)\) micelles were discussed in details in the main text. Homopolymer adsorption, particularly within the corona, is much stronger for the starlike micelle. Both for the crew-cut and starlike micelles, depletion of the homopolymer is reflected on values of \(f_{G_0}^{\text{bulk}}\). Furthermore, at the same intermicelle distance \(r\) depletion effects are clearly stronger for the crew-cut than for the starlike micelle \((f_{G_0} at z=0\) is smaller for the crew-cut micelle for any \(r\)). This relates, once again, to the more diffuse peripheral colloidal domain (corona) of the starlike micelle. With increasing \(f_{G_0}^{\text{bulk}}\), the depletion zones get compressed also when micelles approach each other (except for distances \(r < 2R_h^0\)). In Fig. 11(c) and (d) homopolymer radial volume fraction profiles for adsorption cases are presented. Contrary to the depletion cases, when micelles get close to each other \(f_{G_0} > f_{G_0}^{\text{bulk}}\). While depletion effects are stronger for the crew-cut micelle (near full-depletion for \(r = 2R_h^0\), adsorption effects are clearly more pronounced between starlike micelles.

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