Spatial Mapping of Local Density Variations in Two-dimensional Electron Systems Using Scanning Photoluminescence

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We have developed a scanning photoluminescence technique that can directly map out the local two-dimensional electron density with a relative accuracy of $\sim 2.2 \times 10^8 \text{cm}^{-2}$. The validity of this approach is confirmed by the observation of the expected density gradient in a high-quality GaAs quantum well sample that was not rotated during the molecular beam epitaxy of its spacer layer. In addition to this global variation in electron density, we observe local density fluctuations across the sample. These random density fluctuations are also seen in samples that were continuously rotated during growth, and we attribute them to residual space charges at the substrate-epitaxy interface.

This is corroborated by the fact that the average magnitude of density fluctuations is increased to $\sim 9 \times 10^8 \text{cm}^{-2}$ from $\sim 1.2 \times 10^8 \text{cm}^{-2}$ when the buffer layer between the substrate and the quantum well is decreased by a factor of seven. Our data provide direct evidence for local density inhomogeneities even in very high-quality two-dimensional carrier systems.

Keywords: Molecular beam epitaxy, Photoluminescence, Two-dimensional electron system (2DES), Quantum well, Electron density mapping

Low-disorder two-dimensional electron systems (2DESs) are fundamental components of modern solid state physics research. Long-scale ballistic transport is essential for the operation of quantum devices, and many-body-driven phenomena typically emerge in samples having extremely high quality. Pioneering works to achieve clean 2DESs were performed in GaAs/Al$_x$Ga$_{1-x}$As heterostructures, and they have led to extraordinary achievements such as the discovery of the fractional quantum Hall effect, the observation of ballistic transport, and the realization of exotic many-body states such as a Wigner crystal and nematic/stripe phases. The motivation to obtain better quality 2DESs has also extended to other single-crystal material systems, and several breakthroughs have made electron-electron interactions observable in 2DESs prepared in Si(111), AIA, GaN, CdTe, ZnTe, Ge, and InA. Recent advancements in the quality of 2D materials such as graphene has yielded phenomenal results as well, demonstrated by the observation of unconventional even-denominator fractional quantum Hall states and correlated insulating and superconducting phases.

Inspired by the fruitful outcome of such improvements to 2DES quality, endeavors to fabricate even higher quality samples continue to this day. For example, the primary source of scattering in state-of-the-art GaAs 2DESs is often attributed to background impurities, and to this end there have been several reports on methods to purify the source material. Another possible scattering source is the presence of density inhomogeneities within the 2DES, which have been speculated to cause unwanted effects during measurements. However, in general electrical measurements are too global to detect these inhomogeneities. Previously, we have demonstrated the capability to measure the local 2DES density of a GaAs sample at a fixed location on the wafer using a photoluminescence (PL) technique. Here, we show that we have further developed this method and can now spatially map out the local 2DES density variations over macroscopic regions on the wafer with better than 100 $\mu$m precision. In contrast to earlier studies, where the average density variations were inferred from transport measurements over the entire device, our approach provides a direct and local probe of the 2DES density. We find that density fluctuations on the order of $\sim 10^8$ electrons cm$^{-2}$ exist even in high-mobility samples designed to have uniform 2DES density, which quantitatively supports some of these previous reports.

As described in detail in our previous work, our experiment is set up to extract the local 2DES density of GaAs quantum wells (QWs) placed in a continuous flow cryostat using PL. A 750-nm laser with an intensity of 1.2 $\mu$W focused on a spot size with a diameter of 40 $\mu$m was used to generate the PL signal. In addition, to achieve spatial mapping, the samples were mounted on a contact-cooled, piezoelectric stage whose in-plane movement can be controlled with sub-micrometer precision (Attocube ANC350). In our studies, the minimum spacing between measurements was 100 $\mu$m. All measurements were performed at the base temperature of our apparatus, which was roughly 7 K. Our GaAs QW samples are grown on (001) oriented GaAs substrates by molecular beam epitaxy (MBE), with Si $\delta$-doping only on the surface side of the structure to have an electron density of $n = 2.9 \times 10^{11}$ cm$^{-2}$ and a mobility of $\mu = 6.3 \times 10^6$ cm$^2$ V$^{-1}$s$^{-1}$. A relatively narrow well width of $w = 20.3$ nm was chosen to prevent any possible complications in the Fermi-edge from second sub-band occupation. The thickness of the buffer layer between the substrate and QW is fixed to 1.4 $\mu$m, except for the case where an intentionally thin

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buffer of 200 nm was implemented to amplify effects from the substrate. Figure 1(a) shows a representative PL spectrum of such a GaAs 2DES measured in our system. Gaussian fits to the raw data and the derivative are used to determine the energy positions of the peaks, which correspond to the ground state energy ($E_0$) and Fermi energy ($E_F$), respectively.

Before discussing our data, we describe the terminology used in our measurements. As schematically depicted in Fig. 1(b), all the energy levels, including $E_0$ and $E_F$, are defined with respect to the valence band $E_V$ of GaAs. The 2DES density is deduced by subtracting $E_0$ from $E_F$ and multiplying by the density of states $[n = (E_F - E_0) \times (m^*/\pi\hbar^2)]$. Because the focused spot size of our laser is only 40 $\mu$m in diameter, we can map out the 2DES density on a local scale as the spot is scanned across the sample. For instance, if there are any positively (negatively) charged impurities in the vicinity of a specific area excited for a PL measurement, the spectra would show an increase (decrease) in $E_F$ and hence the 2DES density, as shown in Fig. 1(b). The relative accuracy of our 2DES measurements is $\sim 2.2 \times 10^8$ cm$^{-2}$, which is determined by sampling the local 2DES density at a fixed point on the wafer 10 times and taking the standard deviation. This is comparable to the difference between the local 2DES density values measured at the same position, with a measurement at another point on the wafer in between, which is $\sim 2.9 \times 10^8$ cm$^{-2}$.

In order to verify the validity of our approach, we first grew a GaAs sample that was designed to have a 2DES density gradient of roughly 1%/mm. This was achieved by utilizing the fact that our source ovens are pointed at a 60° angle to the sample growth plane, and stopping the rotation of the wafer only during the growth of the AlGaAs spacer layer. The spacer thickness is therefore varied across the wafer, leading to a density gradient. All other parts of the sample, including the GaAs QW, were grown at a fixed rotation rate of 10 RPM. A schematic diagram that depicts the layer structure of this sample is shown in Fig. 1(c). Figure 2(a) shows a 2DES density contour plot of a 4 mm×1 mm piece of the non-rotated sample. There is a clear density gradient observed across the long axis of the sample, which corresponds to $\sim 4.5\%$ over 4 mm. This is quite close to the 1%/mm variation we expected from our growth conditions, which demonstrates that our approach to spatially map out the density of a 2DES using PL is indeed viable.

A closer inspection of Fig. 2(a) shows that, in addition to the expected global variation of density over the sample, there are also smaller, more local fluctuations in the 2DES density. To analyze this in finer detail we individually examine the spatial variations of the two terms used to deduce the density, $E_F$ and $E_0$, as shown in Figs. 2(b) and (c), respectively. The fluctuations of $E_F$ shown in Fig. 2(b) seem quite random in both position and intensity while the variation of $E_0$ shown in Fig. 2(c) is smooth and continuous. The gradual decrease observed in $E_0$ as the 2DES density increases along the x-axis coincides well with the anticipated effects from band-gap renormalization. Comparing Figs. 2(b) and 2(c), it is clear that most, if not all, of the local fluctuations observed in the density [Fig. 2(a)] come from $E_F$.

This is further confirmed in the PL measurements of a sample that was rotated during the entire growth period, as illustrated in Figs. 2(d)-(f). Figure 2(d) shows the density map of the rotated sample. The global den-
FIG. 2. PL measurement contour maps of 1 mm × 4 mm samples. Each black dot depicts a point where the PL spectrum was measured and analyzed. The spacing between points is 100 µm along both axes. For (a)-(c) the sample was not rotated during the growth of the spacer layer, while (d)-(f) show data for a sample that was rotated at a rate of 10 RPM during the entire growth period. The 2DES density deduced from the difference between the measured $E_F$ and $E_0$ values is shown in (a) and (d). $E_F$ and $E_0$ are plotted in (b), (c) for the non-rotated sample, and in (e), (f) for the rotated sample. As illustrated in (d), density inhomogeneities are quite noticeable even in high-quality samples designed to have a uniform 2DES density. All PL spectra were taken at $T \approx 7$ K.

Density gradient is absent in this sample, but there are still obvious local density inhomogeneities. The data shown here provide a direct measurement of density inhomogeneities in a high-quality GaAs 2DES. In the past, such inhomogeneities have only been inferred indirectly from transport measurements over the bulk of a device.\textsuperscript{29-33} Similar to the non-rotated case, in Fig. 2(e) $E_F$ for the rotated sample shows noticeable local structure with random fluctuations sprinkled throughout the sample. This time, the $E_0$ values plotted in Fig. 2(f) show very little variation across the measured area, consistent with the sample being designed to have a uniform 2DES density. We speculate that the step-like features in Fig. 2(f) come from layer fluctuations during the growth. From Figs. 2(e) and (f), it is again evident that the local density fluctuations mainly stem from changes in $E_F$. As mentioned earlier, because $E_F$ in our experiments is defined from the valence band, the data then imply that there are local charge patches scattered throughout the sample that generate electric fields and result in a non-uniform 2DES density.

We attribute these charge patches mainly to residual impurities at the substrate-epitaxy interface. It is well known that it is difficult to completely remove certain elements such as C, O, and Si from the surface of commercial GaAs substrates even after extended periods of in-situ thermal desorption prior to MBE growth.\textsuperscript{36,37} Alternatively, because the PL measurements were not performed in-situ, there could be unwanted adatoms from the atmosphere that act as either donors or acceptors on the GaAs surface. Residual impurities incorporated in the structure during the MBE growth, as well as crystalline defects such as oval defects or dislocations in the GaAs substrate, may also impact the local 2DES density.

In order to gain more insight on the origin of the density fluctuations, we grew a GaAs sample that has identical spacer thickness and QW width as the sample of Fig. 2(d) but with a factor of 7 thinner buffer layer of 200 nm instead of 1.4 µm between the substrate and the QW. If the local density inhomogeneities originate from the residual charge patches at the substrate-epitaxy interface, the decreased buffer-layer thickness should amplify the effect and cause larger 2DES density fluctuations. Figure 3(a) shows the density map of the sample with a buffer-layer thickness of 200 nm. Compared to the sample with 1.4 µm buffer-layer thickness shown in Fig. 2(d), it is clear that the intensity of local density inhomogeneities is much more pronounced. We can therefore...
FIG. 3. (a) Contour map of local 2DES density for the 200-nm-thick buffer sample. (b) Density map of the same region shown in (a) but after a full thermal cycle. (c) Line profiles of the density contour maps shown in Figs. 3(a) and Fig. 2(d): The colored solid lines correspond to the dashed lines shown in Fig. 3(a) while the black (red) dotted lines correspond to line profiles along the x-axis at y = 100 (900) µm in Fig. 2(d). All PL spectra were taken at T ≃ 7 K.

The linear scaling of the amount of charge depleted as the buffer-layer thickness is decreased strongly supports our conjecture that charged defects are located at the substrate-epitaxy interface and influence the local density structure of a 2DES in a GaAs QW. For the case of depletion, we suspect that C atoms are accountable for this type of density inhomogeneity as they are known to act as acceptors in GaAs. The separation between the depleted regions is on the order of ∼ 100 µm, it is worthwhile to also consider dislocations in the GaAs substrate as a possible source of the local depletion. The specified etch-pit density of wafers typically used for growth in our chamber is 1500 ∼ 5000 cm⁻², which translates to a length scale of 140 ∼ 250 µm. This is comparable to the separation length mentioned above, and we cannot disregard the possibility that acceptor-like charges form at the dislocation sites near the substrate-epitaxy interface and contribute to the depletion observed in our data.

Despite the prominent changes in the degree of depletion as the buffer-layer thickness was decreased, there seems to be much less of an effect for accumulation. As shown in Fig. 3(c), in general the amount of accumulated charge does not show a significant difference for the two samples. Compared to the median value of ∼ 2.95 × 10¹¹ cm⁻², in accumulated regions the thin- and thick-buffer-layer samples typically show an increase of ∼ 2.7 × 10⁹ cm⁻² and ∼ 2.4 × 10⁹ cm⁻², respectively. The density change ratio of 1.13 does not coincide with the factor of 7 decrease in the buffer-layer thickness, which suggests that the accumulation is not related to trapped charges at the substrate-epitaxy interface. We see similar weak and broad accumulation patches even in samples with a buffer-layer thickness of 7 µm, further strengthening this
argument (data not shown). At the moment we are unsure of what causes this type of density fluctuations. As mentioned earlier, it is possible that it is caused by impurities at the GaAs wafer surface or background impurities in the epitaxially grown structure.

Following the discussion in the previous paragraphs, it is interesting to investigate the change in the 2DES density map after the sample experiences a thermal cycle. If the local charge fluctuations in Fig. 3(a) come from fixed charge sources trapped at the substrate-epitaxy interface or other residual impurities in the sample, warming the system up to room temperature and then cooling it back down should have minimal impact on the overall features in the density map. Figure 3(b) shows the density map of the same region probed in Fig. 3(a) after the sample was warmed up to 300 K and cooled down to the base temperature again without breaking vacuum in the sample space. The data appear quite reproducible, showing similar density fluctuations in terms of both position and intensity even after a full thermal cycle.

In conclusion, we have demonstrated a technique that can map out the local density of a 2DES using scanning PL. A GaAs sample with an intended density gradient of ∼1%/mm was grown by MBE and was verified by our PL setup to have a density drop of ∼4 mm piece. In addition to this expected global variation in 2DES density, the density map revealed other, more local, density fluctuations which were also found in a sample grown without any intentional density gradients. We attribute the locally depleted regions to residual acceptor-like impurities at the substrate-epitaxy interface, and our conjecture is supported by the fact that the average local depletion increased from ∼1.2 × 10^9 cm^-2 to ∼9 × 10^9 cm^-2 when the buffer-layer thickness was decreased from 1.4 μm to 200 nm. The position and magnitude of the density fluctuations we observe are quite reproducible even after a full thermal cycle to room temperature, which is consistent with the fact that residual impurities trapped at the substrate-epitaxy interface should not be very mobile. Our data directly show that there are local density inhomogeneities on the order of ∼10^9 cm^-2 even in clean 2DESs, quantitatively corroborating previous speculations based on anomalous features in transport measurements. The technique and results presented here should find use in various topics of 2DES research that cannot be probed by transport measurements on macroscopic samples.

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