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Full Variation of Site Substitution in Ni-Mn-Ga by Ferromagnetic Transition Metals

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Abstract: Systematic doping by transition elements Fe, Co and Ni on each site of Ni2MnGa alloy reveal that in bulk material the increase in martensitic transformation temperature is usually accompanied by the decrease in ferromagnetic Curie temperature, and vice versa. The highest martensitic transformation temperature (571 K) was found for Ni50.0Mn25.4(Ga20.3Ni4.3) with the result of a reduction in Curie temperature by 55 K. The highest Curie point (444 K) was found in alloy (Ni44.4Co5.1)Mn25.1Ga24.9; however, the transition temperature was reduced to 77 K. The dependence of transition temperature is better scaled with the Ne/a parameter (number of non-bonding electrons per atom) compared to usual e/a (valence electrons per atom). Ne/a dependence predicts a disappearance of martensitic transformation in (Ni45.3Fe5.3)Mn25.0Ga24.6, in agreement with our experiment. Although Curie temperature usually slightly decreases while the martensitic transition increases, there is no significant correlation of Curie temperature with e/a or Ne/a parameters. The doping effect of the same element is different for each compositional site. The cascade substitution is discussed and related to the experimental data.

Keywords: Ni-Mn-Ga; doping; ferromagnetism; transition metals; Heusler alloy

1. Introduction

The magnetic shape memory (MSM) effect or magnetically induced reorientation (MIR) observed mostly in Ni-Mn-Ga Heusler alloys provides up to 12% deformation induced by moderate magnetic fields of less than 1 T [1,2]. To obtain this multiferroic behaviour, the material must be ferromagnetic and exhibit martensitic transformation to a ferroelastic state. Moreover, to obtain MIR, the twin boundaries formed upon transition have to be highly mobile [3–7].

Although the MSM phenomenon is extraordinary and unique among all known metallic alloys, there are important issues which hinder its transfer from basic research toward applications. One of the main issues is a temperature limit below which the effect can be utilized. There are two limiting temperatures, the martensitic transformation temperature (Tm) and the Curie temperature (TC), since the magnetically induced reorientation effect relies on a high magnetic anisotropy in the martensite ferromagnetic state. Thus, apart from increasing transformation temperatures, the high mobility of twin boundary and high magnetocrystalline anisotropy must be maintained.

Early studies of ternary Ni-Mn-Ga showed that Tm and TC are in competition with each other [8–11]. Increasing the concentration of Mn at the expense of Ga (Ni50Mn25+xGa25−x) increases Tm but decreases TC until the Curie temperature of the martensitic phase becomes smaller than Tm, at about 7 at. % extra Mn [12,13]. Similar behaviour was found for the Ni50−yMn25−yGa25 system [10]. One way or another, the MSM effect seems to be limited to
353 K at best for the strictly ternary Ni-Mn-Ga alloy [14], which is low, considering the operating condition required by many potential applications, e.g., in the automotive industry.

Since the transition temperatures cannot be increased enough by composition variation within the ternary alloy, a large effort is devoted to increase both temperatures by adding more elements into the alloy. Dopants are usually picked from the class of transition metals, e.g., Cr, Fe, Co and Cu [15–19] or the same group of elements, as Ga is often replaced by In [20] or Sn [21–23]. However, in such kind of substitution, the fulfilment of the conditions for the MSM effect is commonly ignored.

The majority of published papers have reported the substitution of just one of the elements in the parent alloy, i.e., Ni, Mn or Ga, and thus the full potential of the multiple dopants remains hidden. An exception is the work of Soto-Para et al. [15] in which they selectively substituted Fe or Co for each original element of Ni-Mn-Ga. However, the Fe-doped alloys were based on a parent composition of Ni$_{53}$Mn$_{22}$Ga$_{25}$, and the Co-doped parent composition was Ni$_{50}$Mn$_{25}$Ga$_{25}$ (at. %). Although the off-stoichiometry of Fe doped alloys was chosen in order to improve the already high transition temperatures, the effect of Fe itself on the alloy and the compositional doping site is difficult to compare with the doped stoichiometry alloys. Recently, Armstrong et al. used a systematic doping approach, by a few atomic percent of Cu and Fe doping on Ni and Mn sites, in an attempt to increase the transformation temperatures while retaining the 10 M modulated structure [24].

In summary, despite the broadness of the existing literature, there is no simple and systematic approach to transition metal doping or alloying. Moreover, due to different preparation methods, high sensitivity to the precise composition and often not well-defined chemical analyses, it is very difficult to compare results from different authors and to obtain reasonable extrapolations and estimations. In addition, there is an apparently non-monotonous dependence of transformation temperatures on doped element concentration. A strong sensitivity to various often not well-defined parameters, and a necessity to retain specific properties to achieve MSM effects, cause large difficulties for reliable ab-initio predictions [24–26].

In this work, we selected the stoichiometric Ni$_2$MnGa as the initial composition to obtain a well-defined baseline and doped it with three ferromagnetic transition metals. We used the same doping amount of 5 at. %, which is a convenient amount for a direct comparison with calculations, laying between the substitution of one (3.125 at. %) and two atoms (6.25 at. %) of a $2 \times 2 \times 2$ supercell commonly used in theoretical modelling. Each original element was substituted by $X = Fe, Co, Ni$, resulting in a series (Ni$_{45}$X$_5$)Mn$_{25}$Ga$_{25}$, Ni$_{50}$(Mn$_{20}$X$_5$)Ga$_{25}$, Ni$_{50}$Mn$_{25}$(Ga$_{20}$X$_5$) (at. %). In this way, we obtained a set of nine alloys, one of them stoichiometric Ni$_2$MnGa.

In order to simplify the discussion on the effect of doping, we assume that the atom replacement is ideal. Although the doping changed the electronic concentration moderately, we found dramatic changes in martensitic temperatures, while the Curie point was affected much less. Moreover, the selective doping revealed a surprisingly strong site dependence. The complete data sets for all nine alloys can serve as a reference point for advanced ab-initio calculations.

2. Materials and Methods

All the investigated alloys were prepared by the same procedure. Elements with purity of at least 99.9% were arc-melted several times, to ensure good mixing, under an overpressure argon atmosphere using a MAM-1 furnace (Edmund Bühler GmbH, Bodelshausen, Germany). The weight loss upon melting was less than 0.8%, which approximately corresponds to the extra 3% of Mn weight we added in order to balance the Mn evaporation tendency, showing that the resulting composition should be close to nominal. The resulting pellet was cut into two parts, and the larger part was annealed in a sealed glass ampoule with a partial pressure of Ar atmosphere. The heat treatment was run in two steps: First, a high temperature macroscopic homogenization treatment at 1273 K for 24 h, followed by a lower temperature ordering-improvement step at 1073 K, close to the B2 $\rightarrow$ L2$_1$ struc-
tural transition, for 24 h. After that, the samples were quenched in a water bath at room temperature. Polycrystalline samples with dimensions of about 5 mm × 3 mm × 1 mm were cut from the annealed part by a spark erosion machine and roughly polished by SiC grinding paper up to the grid of 2400.

The composition of the samples, listed in Table 1, was evaluated using an energy dispersion X-ray microfluorescence (ED-microXRF) spectrometer Eagle-III µProbe (Roentgenanalytik Systeme GmbH & Co., Taunusstein, Germany). The X-ray is emitted by a Rh tube and accelerating voltage 40 kV. The beam was focused to a spot size of about 50 µm (polycapillary focusing optics) and then detected in an 80 mm² Si(Li) liquid nitrogen cooled detector with a resolution of about 140 eV (at MnKα). The concentrations of the elements were evaluated at 5 spots across the sample by a semiquantitative finite elements method with one standard correction, exhibiting an error of about 0.5 at. %, which is a typical error for the method [27–29].

The precise composition evaluation is a critical issue for MSM alloys. The transition temperatures, especially the martensitic transformation, are extremely sensitive to composition, and even a small deviation from the true composition can produce a misleading error. Hence, considerable caution is necessary when comparing transformation temperatures as a function of composition from various sources.

In our notation of composition, we separate the dopant and receiving sublattice from the rest, e.g., Ni49.9Mn24.6(Ga20.4Co5.1). For the sake of consistency, the Ni in the stoichiometry alloy (Ni45.0Ni5.4)Mn24.6Ga25.0 is separated, too. Throughout the paper, we mark the alloys as Ga20Co5 and Ni45Ni5, respectively. Markings of all alloys and their full compositions are shown in Table 1.

The XRD measurements were made using a PANalytical X’Pert PRO diffractometer (PANalytical, Almeo, Netherlands) equipped with a Co tube, in divergent and parallel beam geometry. Measured pole figures revealed the textured oligocrystalline nature of the samples. Therefore, divergent beam geometry with wide slits was used for the initial phase analysis measurements. For each sample, several scans were measured with different sample orientations suggested by the measured pole figures. This allowed us to collect a sufficient number of reflections for confident phase composition analysis.

Even though no other known phases common for Ni-Mn-Ga-based alloys than those listed in Table 2 were detected in the measured scans and pole figures, due to the measurement-complicating oligocrystalline nature of the samples and practical impossibility to cover the whole space of orientations, there might be a slight chance of the presence of lower amounts of undetected additional phases. This, however, seems to be clearly excluded by magnetic measurement. After the aforementioned measurements,
selected reflections for single grains were measured in the parallel beam geometry for the precise determination of the lattice parameters which are listed in Table 2.

Table 2. Structure and lattice parameters (nm) were determined at room temperature by X-ray diffraction. XRD patterns for all compositions are shown in the Supplemental File.

| Identifier | \(a_0\) | \(a\) | \(b\) | \(c\) | \(\gamma\) | \(c/a\) | Structure |
|------------|--------|--------|--------|--------|---------|--------|-----------|
| Ni\(_{45}\)Fe\(_5\) | 0.5827(1) | – | – | – | 90 | – | A |
| Mn\(_{20}\)Fe\(_5\) | 0.5814(1) | – | – | – | 90 | – | A |
| Ga\(_{20}\)Fe\(_5\) | – | 0.6200(2) | 0.5764(2) | 0.5506(2) | 90.4(2) | 0.89 | 14M |
| Ni\(_{45}\)Co\(_5\) | 0.5822(1) | – | – | – | 90 | – | A |
| Mn\(_{20}\)Co\(_5\) | – | 0.5535(2) | – | 0.6384(2) | 90 | 1.15 | NM |
| Ga\(_{20}\)Co\(_5\) | – | 0.5424(2) | – | 0.6630(2) | 90 | 1.22 | NM |
| Ni\(_{45}\)Ni\(_5\) | 0.5818(5) | – | – | – | 90 | – | A |
| Mn\(_{20}\)Ni\(_5\) | – | 0.5469(4) | – | 0.6515(5) | 90 | 1.19 | NM |
| Ga\(_{20}\)Ni\(_5\) | – | 0.5392(2) | – | 0.6701(1) | 90 | 1.24 | NM |

The magnetic measurements were performed using a physical property measurement system (PPMS) with a 9 T superconducting coil (Quantum Design, Inc., San Diego, CA, USA). We used a vibrating sample measurement regime for magnetization dependence on both the external magnetic field and temperature. Magnetisation vs. field measurements confirm that magnetic saturation is clearly complete by the application of a 2 T field, and so the temperature dependence of saturated magnetization was taken at the constant field of 2 T. The saturation magnetization \(M_{sat}\) and coercive field \(H_C\) were determined from the magnetization curves, as shown in Figure 1 for two alloys. Since the martensitic and austenitic phases strongly differ in their magnetic properties, the phases can be easily distinguished from the different shape of the magnetization curves, where the greater anisotropy of the martensite phase shows a harder ferromagnetic \(M/H\) response.

![Magnetization curves](image-url)

**Figure 1.** Isothermal magnetisation curves of (a) \((\text{Ni}_{45.0}\text{Ni}_{5.4})\text{Mn}_{24.6}\text{Ga}_{25.0}\) and (b) \((\text{Ni}_{49.9}\text{Mn}_{24.6})(\text{Ga}_{20.4}\text{Co}_{5.1})\).

Owing to its high sensitivity, low-field thermomagnetic measurement (\(\mu_0H = 10\) mT) was used to determine all transition temperatures: Curie temperature \(T_C\), premartensitic transition \(T_{pm}\), martensite start and finish temperatures \((M_s, M_f)\) and austenite start and finish temperatures \((A_s, A_f)\), respectively. From the last four temperatures, the single value, equilibrium martensitic transition temperature \((T_m)\) was calculated as 
\[T_m = (M_s + M_f + A_s + A_f)/4.\]

The transition temperatures were determined from the low-field thermomagnetic curves as the intersection of two extrapolated lines, one of the
maximal slope and one of the minimal slope, as shown in Figures 2 and 3. This method of transition temperature determination is common and straightforward [17,19,21,30]. The precision of the method is acceptable if the DC magnetic susceptibility or low-field magnetization measurement changes steeply in a narrow temperature range. The sharp change is common in high-quality Ni-Mn-Ga single crystals [31], and although we studied polycrystalline samples, the transition was still very steep.

Figure 2. Low-field and saturation magnetization, measured at constant magnetic field $\mu_0 H$ of 0.01 T and 2 T, respectively, as a function of temperature: (a) (Ni$_{45.0}$Ni$_{5.4}$)Mn$_{24.6}$Ga$_{25.0}$ exhibiting Curie temperature $T_C$, premartensitic transition $T_{pm}$ and martensitic transformation $T_m$ marked in the figure; (b) Ni$_{49.9}$Mn$_{24.6}$(Ga$_{20.4}$Co$_{5.1}$) exhibiting a martensitic transformation above $T_C$ of martensite.

On the other hand, the Curie temperature determination depends on the method used. For example, the $T_C$ of the Ni$_{45}$Fe$_5$ (full composition in Table 1) alloy determined by the tangent method, i.e., by slope extrapolation to zero magnetization, and by inflexion point (both of the low-field thermomagnetic curves) and by the Arrott plot [32,33] gives 399 K, 394 K and 403 K, respectively. In addition to these methods, we can determine the paramagnetic Curie temperature from a plot of reciprocal magnetization vs. $T$ by extrapolation to zero, which gives 396 K. For consistency, we used the method of the tangents crossing for all data evaluation. Importantly, we corrected the thermomagnetic measurements for the temperature rate (4 K/min) in order to obtain the most precise transition temperatures possible. Detailed thermomagnetic curves for all samples can be found in the supplementary files.

The $e/a$ parameter represents average number of valence electrons per atom in one formula unit. This parameter is commonly used in the field, as part of a broad common theme of valence electron counting in Heusler compounds [34]. Nevertheless, for the sake of completeness the exemplary enumeration is provided. The number of valence electrons
for Ni, Mn, Ga, Fe, Co are 10, 7, 3, 8, 9, respectively, and the parameter $e/a$ for the particular alloy with experimentally determined composition Ni$_{49.9}$Mn$_{24.6}$(Ga$_{20.4}$Co$_{5.1}$) is calculated as follows:

$$e/a = \frac{(10 \times 49.9 + 7 \times 24.6 + 3 \times 20.4 + 9 \times 5.1)}{100} = 7.78$$

(1)

Although the $e/a$ ratio is widely used as a parameter to compare alloys of different composition, in the doped systems of Ni-Mn-Ga it becomes more complicated and anomalous behaviour appears as shown already by Ramudu et al. [35]. They introduced new parameter $N_e/a$ and demonstrated its benefits over the $e/a$, e.g., the $N_e/a$ provides the trend of $T_m$ in the case of constant $e/a$ for different compositions of Ni-Mn-Ga-In alloys. Another argument supporting the use the $N_e/a$ is given later in this paper. The $N_e/a$ parameter stands for an average number of non-bonding electrons per atom in one formula unit or so-called effective valence electrons [35]. The expression is given by the formula

$$N_e/a = E - N_{WS},$$

where $E$ is number of valence electrons and $N_{WS}$ originates from the empirical model of Miedema et al. and is defined as the electron density at the boundary of the Wigner-Seitz cell [36,37]. The number $N_{WS}$ is derived from molar volume and bulk modulus of the particular element. For the elements discussed in this work, we use non-bonding electron counts, $N_{WS}$, of 5.36, 4.17, 2.25, 5.55 and 5.36, for Ni, Mn, Ga, Fe and Co, respectively [35,36]. The $N_e/a$ outcome is then enumerated similarly to $e/a$, for the same alloy Ni$_{49.9}$Mn$_{24.6}$(Ga$_{20.4}$Co$_{5.1}$):

$$N_e/a = [(10 - 5.36) \times 49.9 + (7 - 4.17) \times 24.6 + (3 - 2.25) \times 20.4 + (9 - 5.36) \times 5.1]/100 = 3.40,$$

(2)

Both parameters $e/a$ and $N_e/a$ together with the experimentally determined compositions for all prepared alloys are listed in Table 1.

3. Results

It should initially be stated that all replacements mentioned in the text strictly refer to chemical composition replacement. Additionally, we assume that the atom replacement is ideal, i.e., the substitution occurs on the atomic position of the original atom. The case of possible sequential or cascade replacement, i.e., the atoms of one element push into another sublattice, is discussed in the last section.

All doping (alloying) and comparisons are related to the very-close-to stoichiometric (Ni$_{45.0}$Ni$_{5.4}$)Mn$_{24.6}$Ga$_{25.0}$ alloy, further on referred to as the stoichiometric alloy.

As an example, we present several figures of selected alloys in the following section to illustrate magnetic behaviour and data evaluation. The complete set of measured data and figures are provided in the supplementary files.

3.1. Transformation Temperatures and Magnetic Properties

In Figure 1, two examples of magnetization curves are displayed, Ni$_{45}$Ni$_{5}$ and Ga$_{25}$Co$_{5}$. For the stoichiometric sample, the magnetization curves clearly demonstrate the difference between magnetically soft austenite and high-anisotropy martensite. On the other hand, although the Ga$_{25}$Co$_{5}$ sample exhibits a martensitic phase at both temperatures, the magnetization curves strongly differ. The difference simply demonstrates how the magnetization curve is skewed close to the Curie point. In the austenite state and in the vicinity of the Curie point, the coercive force is negligible due to the vanishing magnetic anisotropy.

From the comparison of the curves at 10 K, it follows that the Co-doped alloy exhibits a much lower saturation magnetization and also a lower magnetocrystalline anisotropy in the martensite state. The parameters determined from the magnetization curves for all prepared alloys are summarized in the Table 3.

Transformation temperatures were determined from thermomagnetic measurements; see Table 4. The examples of the measurements for the above discussed alloys are shown in Figure 2. In addition, the detection of a martensitic structural transition above the Curie point from the magnetic measurement is demonstrated in Figure 3. To confirm the transfor-
metals indicated by thermomagnetic measurements, differential thermal analysis was also performed. A reciprocal magnetization determined from thermomagnetic measurement is depicted to demonstrate its ability to detect martensitic transition (MT) in the paramagnetic state, which broadens its use to a wider range of alloys, e.g., in paramagnetic NiTi [38] and even in diamagnetic Cu-Ni-Al [39]. The measured thermomagnetic and magnetization curves for all samples are provided as supplementary information.

Table 3. Parameters determined from magnetization curves: saturation magnetization $M_{\text{sat}}$ at 10 K and 300 K at 9 T; coercive force $\mu_0 H_C$ at 10 K and 300 K. The values corresponding to austenitic phase are marked by upper-left corner symbol $\uparrow$.

| Identifier   | $M_{10\text{K}}$ | $M_{300\text{K}}$ | $\mu_0 H_{10\text{K}}$ | $\mu_0 H_{300\text{K}}$ |
|--------------|------------------|------------------|-------------------------|-------------------------|
|              | Am$^2$/kg        | $\mu_B$/f.u.     | mT                      | mT                      |
| Ni$_{45}$Fe$_5$ | 89.0             | 3.85             | 1.7                     | 67.6                    | 1.9                     |
| Mn$_{20}$Fe$_5$ | 91.4             | 3.96             | 12.2                    | 72.0                    | 1.8                     |
| Ga$_{20}$Fe$_5$ | 73.8             | 3.16             | 43.4                    | 64.4                    | 29.3                    |
| Ni$_{45}$Co$_5$ | 97.2             | 4.21             | 0.8                     | 80.3                    | 2.0                     |
| Mn$_{20}$Co$_5$ | 79.6             | 3.46             | 10.9                    | 63.4                    | 7.3                     |
| Ga$_{20}$Co$_5$ | 51.7             | 2.22             | 28.7                    | 30.8                    | 1.3                     |
| Ni$_{45}$Ni$_5$ | 95.1             | 4.12             | 30.2                    | 70.9                    | 1.0                     |
| Mn$_{20}$Ni$_5$ | 76.7             | 3.33             | 28.2                    | 57.0                    | 14.6                    |
| Ga$_{20}$Ni$_5$ | 56.9             | 2.44             | 48.5                    | 34.1                    | 0.9                     |

Table 4. Transition temperatures (K) determined from thermomagnetic measurement: martensite start and finish temperatures ($M_s$, $M_f$), and austenite start and finish temperatures ($A_s$, $A_f$). From these four temperatures, the single value, equilibrium martensitic transition temperature ($T_m$) was calculated using formula $T_m = (M_s + M_f + A_s + A_f)/4$; Curie temperature $T_C$ of martensite is marked $^\dagger$; otherwise, it is austenitic $T_C$, and an apparent Curie point is marked $^\ddagger$ and discussed in Section 3.4.2; $T_{pm}$ indicates premartensitic transition temperature.

| Identifier   | $M_s$ | $M_f$ | $A_s$ | $A_f$ | $T_m$ | $T_C$ | $T_{pm}$ |
|--------------|-------|-------|-------|-------|-------|-------|-------|
| Ni$_{45}$Fe$_5$ | –     | –     | –     | –     | –     | 399   | –     |
| Mn$_{20}$Fe$_5$ | 187   | 170   | 177   | 195   | 182   | 411   | 201   |
| Ga$_{20}$Fe$_5$ | 325   | 318   | 325   | 333   | 325   | 396   | –     |
| Ni$_{45}$Co$_5$ | 104   | 100   | 43    | 61    | 77    | 444   | 151   |
| Mn$_{20}$Co$_5$ | 322   | 309   | 319   | 330   | 321   | 395   | –     |
| Ga$_{20}$Co$_5$ | 541   | 520   | 553   | 597   | 553   | 304*  | –     |
| Ni$_{45}$Ni$_5$ | 205   | 200   | 206   | 212   | 206   | 380   | 258   |
| Mn$_{20}$Ni$_5$ | 382   | 358   | 366   | 384   | 373   | 373*  | –     |
| Ga$_{20}$Ni$_5$ | 564   | 497   | 603   | 621   | 571   | 325*  | –     |

Saturation magnetization, Curie and martensitic transformation temperatures, and $e/a$ and $N_e/a$ parameters for all samples, are summarized in Figure 4. The three main columns are plotted with respect to the doping element, and within each column, the results relate to the original element. The valence electron per atom $e/a$ criterion is usually used for evaluating the effect of doping. It seems that this criterion is broadly valid but not precise as pointed out before. Therefore, we used the new criterion $N_e/a$, as described in the Experimental Section 2, considering the amount of non-bonding electrons per atom [35,36].

In general, the martensitic transformation temperature increases broadly with increasing $e/a$, but the rate of increase cannot be effectively predicted. Moreover, the Curie temperature has a non-monotonous dependence similar to saturation magnetization $M_{\text{sat}}$. In the following, we briefly describe the differences of the magnetic behaviour affected by the substitution of individual elements Fe, Co, and Ni.
Figure 4. Transition temperatures dependence on composition. The full alloy compositions are shown in Table 1. The relative shift compared to stoichiometry alloy Ni\textsubscript{45}Ni\textsubscript{5} is marked by arrows. The transformation temperatures of stoichiometry alloy are marked by dashed lines. In addition, saturation magnetization $M_{\text{sat}}^{300K}$, valence electrons per atom $e/a$ and effective valence electrons per atom $N_e/a$ parameters are shown for comparison.

3.2. Fe Substitution
3.2.1. Ni\textsubscript{45}Fe\textsubscript{5}

The compositional replacement of Ni with Fe increased $T_C$, compared to stoichiometric Ni\textsubscript{45}Ni\textsubscript{5}, but totally suppressed the martensitic transformation as the thermomagnetic measurement and magnetization curves down to 10 K provided no evidence of the transformation.

The austenitic structure was confirmed by X-ray diffraction at room temperature. The saturation magnetization of austenite $M_{\text{sat}}^{300K}$ is smaller than that of the stoichiometric alloy. Coercive force $H_{C}^{300K}$ (1.9 mT) is at the same level as all austenitic phases, except the stoichiometric alloy for which the $H_{C}^{300K}$ is much lower (1 mT). The increase in hysteresis compared to the stoichiometric sample can be explained by a slight local deformation of the structure due to the new element and increasing disorder, which can subsequently result in a higher amount of pinning points for magnetic domain walls [40,41].

3.2.2. Mn\textsubscript{20}Fe\textsubscript{5}

The replacement of Mn with Fe decreases the $T_m$ by 24 K to 182 K and increases $T_C$ by 31 K to 411 K, compared to the stoichiometric alloy, which has the second highest Curie temperature found in this set of alloys. The Mn\textsubscript{20}Fe\textsubscript{5} is the only doped alloy which exhibits a doubtless premartensitic transition, indicated by the thermomagnetic curve. The premartensitic transition was detected at a lower temperature and much closer to the martensitic transition than in the stoichiometric alloy exhibiting such transformation.

The saturation magnetization at 10 K is slightly smaller compared to the stoichiometric alloy, but it is the highest out of all Mn-deficient alloys. The $H_{C}^{10K}$ = 12.2 mT in the martensite phase is less than half of that of the stoichiometric alloy. The $H_{C}^{300K}$ of austenite was already discussed for Ni\textsubscript{45}Fe\textsubscript{5} above, and the same is valid here. Except for $H_{C}^{10K}$, the magnetic properties are very similar to Ni\textsubscript{45}Ni\textsubscript{5}.

3.2.3. Ga\textsubscript{20}Fe\textsubscript{5}

The substitution of Ga with Fe results in a major increase in $T_m$ by 119 K to 325 K and moderate increase of $T_C$ by 16 K to 396 K. This alloy is one of only two alloys in the set
which exhibits an increase in both $T_m$ and $T_C$ at the same time. Additionally, the increase is the largest observed.

Saturation magnetization at 10 K ($M_{\text{sat}}^{10\text{K}}$), however, is the lowest compared to the Fe-doped alloys and moderate among all alloys. The $14\text{M}$ phase was expected to be preserved to 10 K as no intermartensitic transformation was detected. The value of $M_{\text{sat}}^{300\text{K}}$ is the highest among samples in a martensite state owing to the high $T_C$ but is still the lowest when compared to the austenites.

Overall, the Fe substitution causes an increase in $T_C$ for all three alloys. Apparently, the introduced Fe strengthens the ferromagnetic coupling and thus stabilizes the ferromagnetic order of austenite.

### 3.3. Co-Substitution

#### 3.3.1. Ni$_{45}$Co$_5$

Replacing 5 at. % of Ni with Co results in a significant change in both transition temperatures. The Curie temperature increases by 64 K to 444 K. This value of $T_C$ is the highest of the set of alloys. Furthermore, the absolute increase in $T_C$ from the stoichiometric alloy is almost twice as large as the Mn$_{20}$Fe$_5$, which exhibits the second highest $T_C$.

On the other hand, the martensitic transformation temperature $T_m$ is very low, the lowest detected. It appears at 77 K which is 129 K below the $T_m$ of the stoichiometric alloy. The $14\text{M}$ phase was expected to be preserved to 10 K as no intermartensitic transformation was detected.

The alloy exhibits the highest $M_{\text{sat}}^{10\text{K}}$ and $M_{\text{sat}}^{300\text{K}}$ of all alloys. The $H_{\text{C}}^{10\text{K}} = 0.8$ mT is extremely low compared to other samples in martensitic phases; it is even lower than all samples in an austenitic phase exhibited at 300 K.

#### 3.3.2. Mn$_{20}$Co$_5$

The substitution of Mn with Co results in an increase in both transition temperatures, $T_m$ strongly and $T_C$ slightly compared to the stoichiometric alloy. Such coupled behaviour is rare and appears only in the Ga$_{20}$Fe$_5$ alloy. The rest of the alloys exhibit opposing trends in transition temperature. Interestingly, the transformation temperatures for Ga$_{20}$Fe$_5$ are almost identical, but the alloys differ in $e/a$. This demonstrates the limited validity of the $e/a$ comparison approach. On the other hand, their $N_e/a$ parameters differ. Compared to Ni$_{45}$Co$_5$, the coercive force $H_C$ increased quite significantly, and it is comparable to that of Mn$_{20}$Fe$_5$.

#### 3.3.3. Ga$_{20}$Co$_5$

Placing Co in the composition instead of Ga causes a significant increase in $T_m$ by 347 K to 553 K, which is the second highest $T_m$ in the set. However, the Curie temperature strongly decreases by 76 K to 304 K, and appears in the martensitic phase ($T_M$). The $M_{\text{sat}}^{10\text{K}}$ is the lowest and nearly half that of Ni$_{45}$Co$_5$. The coercive force $H_{\text{C}}^{10\text{K}}$ is at a maximum, while $H_{\text{C}}^{300\text{K}}$ is very low for martensite, which is due to the vicinity of the Curie point.

### 3.4. Ni Substitution

#### 3.4.1. Ni$_{45}$Ni$_5$

The substitution of Ni for Ni obviously results to the stoichiometric alloy Ni$_{50.4}$Mn$_{24.6}$Ga$_{25.0}$, or in consistent marking (Ni$_{45.0}$Ni$_{5.4}$)Mn$_{24.6}$Ga$_{25.0}$ (at. %). The measured composition is very close to stoichiometry, and the transition temperatures are in agreement with the generally accepted $T_m$ and $T_C$ [42,43]. Saturation magnetization at 10 K of this alloy is the second highest in the set as the stoichiometric alloy is purely ferromagnetic [44]. The coercive field of austenite at 300 K is almost half when compared to the doped alloys in the austenitic phase. Increased coercivity in some doped alloys suggests that the doping elements may locally deform the cubic lattice providing more pinning points which hinder the magnetic domain wall motion resulting in a higher coercive force than the dopant-free stoichiometric alloy.
3.4.2. Mn$_{20}$Ni$_{15}$

Placing additional Ni instead of Mn causes a significant increase in $T_m$ by 167 K to 373 K, close to the Curie point. In this alloy, it is apparent that the Curie point and MT temperature coincide. The coalescence of $T_m$ and $T_C$ has been found in various compositions of Ni-Mn-Ga [10] or Ni-Mn-In- and Ni-Mn-Sn-based alloys [45,46], often coined as a metamagnetic transition. Entel et al. ascribed the effect to large volume magnetostriction in the vicinity of magnetic phase transition [10]. From our perspective, the phenomenon is simple. If the Curie temperature of martensite $T^M_C$ is above $T_m$ and the Curie temperature of austenite $T_C$ lies below $T_m$ [47], then during cooling, when crossing the martensitic transition, the paramagnetic austenite transforms directly to the ferromagnetic martensite, which has a higher Curie point. This causes the appearance of magnetic order simultaneously with the martensitic transition and apparent Curie point. During heating, the ferromagnetic martensite transforms upon MT directly to paramagnetic austenite, resulting in hysteresis of the Curie point. Thereby, the MT creates an apparent Curie temperature as the paramagnetic austenite undergoes the martensitic transformation to ferromagnetic martensite.

3.4.3. Ga$_{20}$Ni$_{15}$

The substitution of Ga with Ni increases $T_m$ dramatically by 365 K up to 571 K, which is the highest martensitic transformation temperature detected in the set. The Curie temperature decreases again and is exhibited in martensite phase ($T^{MP}_C$) at 325 K, which is 55 K below the $T^{ba}_C$. This makes it the second lowest Curie point in the set. In comparison with the Ga$_{20}$Co$_5$ alloy, this alloy exhibits a similar temperature decrease, i.e., both Ni and Co exhibit similar effect when substituted for Ga. The $M^{10K}_s$ is the second lowest and almost half that of the highest value, which is Ni$_{45}$Co$_5$, and the stoichiometric alloy. The coercive force at 10 K is the highest and at 300 K the lowest of all alloys. The value at 300 K is so low due to the proximity of $T^M_C$ and low easy plane anisotropy of NM martensite. On the contrary, $H^{10K}_C = 48.5$ mT is unusually high for NM martensite, and the closest one is Ga$_{20}$Fe$_5$, which is expected to be 14 M martensite at 10 K.

4. Discussion

Thanks to consistent doping by transition elements in all positions, we can test the predictive power of the widely used $e/a$ and recently introduced $N_e/a$ criteria for transition temperatures. Figure 5 shows the absolute values of transition temperatures $T_m$, $T_C$ and $T_{pm}$ with respect to (a) $e/a$ and (b) $N_e/a$ parameters. A better linear fit, i.e., statistically more significant, of $T_m$, is provided by the $N_e/a$ dependency, and the premartensitic transformation temperature is also well correlated, although we have only three points. Despite the error in the chemical analysis, about 0.5 at.%, the martensitic transition temperatures of all alloys fall into a single line, $T_m = 2130 \times N_e/a - 6739$, as shown in Figure 6. Moreover, a linear fit allows the estimation of the possible $T_m$ of the (Ni$_{45}$Fe$_5$) alloy. The extrapolation based on the $e/a$ parameter gives $T_m = 1222 \times e/a - 8996 = 31.5$ K, while using the $N_e/a$ parameter suggests that there is no martensitic transformation (Figure 6), in agreement with our experimental result. From this perspective, the $N_e/a$ parameter has better predictive power than the $e/a$ ratio. On the other hand, the $T_C$ is scattered and does not exhibit a clear correlation with either parameter.

Although one can expect that the saturation magnetization $M_{sat}$ depends mostly on Mn content, the experiment shows different results. Despite the complex behaviour depending on specific site doping, the general trend is that saturation magnetization decreases with increasing electronic concentration $e/a$, exhibiting an approximate maximum for stoichiometric alloy, i.e., in an ideal L2$_1$ ordered structure. The dependence is shown in the supplementary information. Moreover, the $e/a$ parameter leads to a slightly better linear fit than $N_e/a$. 

![Figure 6](image-url)
Figure 5. Premartensitic ($T_{pm}$), martensitic ($T_m$) and Curie ($T_C$) transition temperatures as (a) a function of number of valence electrons per atom ($e/a$) and (b) a function of number of non-bonding electrons per atom ($N_e/a$). Linear fit of $T_m$ is well correlated to both $e/a$ and $N_e/a$; $T_C$ does not exhibit a good linear fit.

Figure 6. Martensitic transformation temperatures as a function of non-bonding number of electrons per atom $N_e/a$. The marked vertical line corresponds to the (Ni$_{45.3}$Fe$_{5.3}$)Mn$_{23.8}$Ga$_{25.6}$ alloy exhibiting no martensitic transition with $N_e/a = 3.1$. Linear fit of the data provides a formula $T_m = 2130 \times N_e/a - 6739$ intersecting the value 3.1 below 0 K.

Most of the experimental studies of doped Ni-Mn-Ga have selectively substituted just one of the original elements, e.g., [16,19,48–50]. At first approximation, it is a valid approach to introduce a new element in order to study its effect on transition temperatures. However, as we have shown, it is not sufficient. The dopant placing in the composition is crucial and significantly affects the transition temperatures, which is discussed further in the text.

For Fe-doped alloys, Soto-Para et al. [15] prepared a similar full doping series substituting all original elements. However, the Fe-doped Ni-Mn-Ga series were based on the off-stoichiometric parent Ni$_{53}$Mn$_{22}$Ga$_{25}$ alloy, with an Fe content from 0 to 5 at. %. Since the base alloy exhibits significantly different transition temperatures from the stoichiometric one, the direct comparison with this work is difficult; however, the general trends are consistent. In agreement with their reasoning [15], the effect of Fe doping is to enhance magnetic exchange coupling and thus increase $T_C$. The doping by Fe, on the other hand, apparently caused a decrease in the free energy difference between the austenite and martensite phases, resulting in the stabilization of the austenitic parent phase, i.e., decreasing the $T_m$. 
Similarly, the Co-doped series from the same paper [15] is based on the stoichiometric alloy as the reference system, which enables a direct comparison, and the trends again agree very well. Although the absolute values are not provided but estimated, the Curie temperatures $T_C$ seem to be in better agreement than the martensitic temperatures $T_m$. This may not be surprising as $T_m$ is much more sensitive to composition. Moreover, Soto-Para et al. used the martensite start temperatures ($M_s$), while our approach utilized the equilibrium martensitic temperature $T_m$. When making similar comparisons using $M_s$ (supplementary information), our trends are clearly comparable within, a discrepancy which can be confidently ascribed to composition variation between our alloys and the composition determination error.

Until now, we discussed how the new elements affect the transformation temperatures $T_m$ and $T_C$, as summarized in Figure 4. Additionally, we showed that if the dopant is placed into various compositional sites, the transition temperatures follow broadly the same trend, regardless of which new element is introduced. This can provide an alternative perspective related to the reduction in the original element contrasting the introduction of a new one.

Following this idea, we rearranged the obtained results with respect to the deficiency of the original elements; see Figure 7. This immediately shows that if Ni is deficient, $T_m$ decreases strongly and $T_C$ increases significantly, irrespective of the substituting element. This trend was also observed in [16,48,51] for Co or in [52] for Fe.

![Figure 7. Transition temperatures dependences on composition rearranged according to a doping site.](image)

In addition, saturation magnetization $M_{sat}^{10K}$ and $c/a$ and $N_{c}/a$ parameters are plotted for comparison. The dashed lines mark transition temperatures of the stoichiometric alloy, and the arrows emphasize a temperature deviation from them.

On the other hand, if Ga is deficient, the effect is almost opposite and very steep, $T_m$ increased and $T_C$ decreased, except for Ga$_{20}$Fe$_{5}$, where the $T_C$ also slightly increased. Such trends are not unique and can be found in other works [15,30,53,54]. Surprisingly, the substitution of Ga by ferromagnetic metals results in a strong decrease in magnetic moment, possibly due to antiferromagnetic coupling with the major magnetic moment on Mn atoms.

The Mn-deficient alloys do not exhibit a clear trend, two out of three alloys show an increase in $T_C$ and a different two show an increase in $T_m$. In ternary Ni-Mn-Ga, the deficiency of Mn leads to an opposite effects depending on whether the composition is Ni- or Ga-rich. The Mn$_{20}$Fe$_{5}$ exhibits a similar trend of transition shift to Ga-rich alloys [55,56] and Mn$_{20}$Co$_{5}$ and Mn$_{20}$Ni$_{5}$ to Ni-rich alloys [10,57]. Although the effect on Mn-deficient
alloys is not monotonous and depends on the doping element, our data are in agreement with previous reports, e.g., Mn$_{20}$Fe$_5$ with [58], Mn$_{20}$Co$_5$ with [18,51,59] and Mn$_{20}$Ni$_5$ with [10,57]. It seems that the effects of the doping element is minor compared to the Mn-deficiency itself.

In reality, substitutions may not be ideal, as assumed, and the dopant may prefer another sublattice than the intentionally vacant one. Then, the dopant may push the original atoms from their own preferred lattice site into the vacant one, and this can start a cascade of substitutions between the particular sublattices. The cascade means that, e.g., Co is supposed to compositionally replace Ga written as a Ni$_{50}$Mn$_{25}$(Ga$_{20}$Co$_5$) alloy, but in fact, the Co atoms tend to occupy, for instance, the Mn sublattice, and the Mn atoms are pushed into the vacant Ga sublattice forming the Ni$_{50}$(Mn$_{20}$Co$_5$)(Ga$_{20}$Mn$_5$) alloy. We call this type a cascade of a first order.

Of course, if we extend the idea one step further from the first-order cascade, it results into the second-order cascade. If in the previous example Co would prefer the Ni sublattice, the expelled Ni would prefer the Mn sites, and Mn must settle in the vacant Ga sublattice; the composition formula could be then written according to the preferential sites as (Ni$_{45}$Co$_5$)(Mn$_{20}$Ni$_5$)(Ga$_{20}$Mn$_5$).

It is difficult to determine preferential sites experimentally. The similarities in X-ray scattering factors result in very little contrast between these elements with such close electron numbers. Neutron diffraction can provide an enhanced contrast, but the possibility of refining the occupancy of three elements on a single site requires the careful use of either multiple data sets from different radiation types, or careful imposed constraints that must be reasonably justified.

Richard et al. studied four Ni-Mn-Ga compositions from which three were powdered single crystals and one was maintained for single crystal diffraction [60]. The best model fitting the neutron diffraction data suggested that excess Mn atoms tend to occupy Ni and Ga sites and no cascade occurs. On the other hand, for the Ni-rich alloy, the atoms expel the Mn into the Ga sites, i.e., the first-order cascade, resulting in enhanced ferromagnetic (FM) coupling on the Mn sites, and enhanced antiferromagnetic (AFM) coupling on the Ga sites.

For the doped Ni-Mn-Ga alloy, there are three neutron diffraction reports which deal with the site preference. In the report by Porro-Azpiazu et al., they studied the Ni$_{51}$(Mn$_{28-x}$Y$_x$)Ga$_{21}$ (Y = Fe, Co) system but other than the available experimental report, the results have not been published as a peer reviewed article [61]. A more complicated system of (Ni$_{50}$Co$_{50}$)(Mn$_{25-x}$Fe$_x$)(Ga$_{20}$Cu$_5$) ($x = 0, 1, 2, \ldots, 6$ and 8) was studied by Lazpita et al. mostly on powder samples prepared from single crystals [62]. Although their intention was obviously to replace the original elements by the particular ones as marked, the dopants were found in different sites (for $x = 1$), resulting in complex situation: Cu in Mn sites, which expels Mn into Ga and Ni sites; Co in Ga sites; Fe in Ni and Mn sites. The following report from two single crystals of compositions $x = 4$ and 5 confirmed the aforementioned results [63]. However, these reports have also not yet been published, apparently due to the complex nature of the substitution, and the required complexity of the analysis. Although one can expect that different elements favour specific sublattices, firm evidence is still missing.

Since the site preference is difficult to study experimentally, and an insufficient amount of data has so far been provided, we resort to reported ab-initio calculations [64,65]. Li et al. [64] showed that on a system doped by 1.25 at. % of Fe, Co or Cu, the energetically preferable sites for Fe are Ni and Mn sublattices when they are vacant. Rather than to settle in a Ga vacant sublattice, Fe causes a cascade with Mn expelled into the Ga sublattice. However, the calculated energy of the cascade is only slightly more preferable than that of the cascade with Ni or the no cascade system. As the difference between calculated energies is not conclusive at all, it means one should be able to find Fe in Ga sites at least up to 1.25 at. %. This correlates with the neutron diffraction report by Perez-Checa et al. [63] in which they found 0.5 at. % of Fe in the Ga sublattice out of 5.25 at. % doping.
It may be that only a small amount of Fe can be incorporated into the Ga sublattice, and the rest settle in Mn and Ni sites. However, their studied system, having three different dopants, is complex, and the reported settlement may be a product of this complexity or disorder.

The results presented here indicate the first-order cascade with Mn sites and the combined effect of both Fe and Mn on their doping sites. Fe in the Mn sublattice results in a minor decrease in $T_m$ and a major increase in $T_C$, as shown in Figure 4, and may substitute Mn adequately, as they have similar atomic radii. Expelled Mn in the Ga sublattice causes a steep increase in $T_m$ and a slight decrease in $T_C$, which is widely known from the Mn-rich Ni$_2$MnGa. Both effects combined may result in transition temperatures found in the Ga$_{20}$Fe$_5$ alloy.

For the Co doped system, Li et al. [64] showed by ab-initio calculations that Co atoms tend to occupy the Ni sublattice in every scenario and push Ni atoms into the vacant sublattice. The second-order cascade, i.e., Co expelling Ni and Ni expelling Mn, is not energetically preferred as much as the first-order cascade, according to Li et al. This partially disagrees with the experimental data of Richard et al. [60] and calculations of Jie et al. [65], both conducted on a Ni-rich Ni-Mn-Ga alloy, showing that extra Ni prefers Mn sites. Therefore, the second-order cascade could appear in the Co-doped Ga-deficient alloys.

Moreover, a relatively simple quantitative model was proposed by Ayila et al. [66]. They studied the occupancy of Co and Fe in a Ga-deficient Ni-Mn-Ga alloy by the calculation of magnetic moment in several occupancy and magnetic order configurations. They showed that both Fe and Co prefer to settle in the filled Mn-Mn-Ga alloy by the calculation of magnetic moment in several occupancy and magnetic order configurations. They showed that both Fe and Co prefer to settle in the filled Mn sublattice, and to align their magnetic moment parallel to the overall ferromagnetic moment of Mn and Ni atoms. The displaced Mn occupies the vacant Ga sites with AFM aligned magnetic moment. Both Fe and Co atoms begin the cascade substitution which is for Fe in agreement with ab-initio calculations [64] and neutron diffraction report [63] but in disagreement for Co. Although the proposed mechanism is in agreement with our experiment, i.e., the saturation magnetization of alloys doped on Ga sites are the lowest, it is inconclusive to ascribe the observed sharp decrease to only Mn antiferromagnetically ordered in Ga position.

When we apply the model of Ayila et al. [66] to our data, it suggests that at least the first-order cascade takes place for the Ga-deficient alloys. Doping the Ni-deficient alloys indicates that Fe and Co tend to settle on the Ni sites being FM coupled. The predicted values for Mn-deficient alloys differ for each case. Fe may settle directly in the Mn sublattice and couple FM, Ni may also settle directly on the Mn sites but couple AFM, which disagrees with the neutron diffraction experiment [60]. In the case of Co, the best correlation with experimental values gives the first-order cascade when Co (FM) pushes Ni into the Mn sublattice, coupled AFM again. This kind of modelling, though, is critical in tuning the parameters close to the experimental values. In order to receive a better fit for some alloys, the elements would need to be mixed much more, and some sort of collective moment should be added.

5. Conclusions

By consistent and selective doping using transition elements (5 at. %) to stoichiometric Ni$_2$MnGa, the highest Curie temperature $T_C = 444$ K was achieved in the (Ni$_{44.9}$Co$_{5.1}$)Mn$_{25.1}$Ga$_{24.9}$ alloy. This alloy, however, exhibited the lowest martensitic transition temperature $T_m = 77$ K detected. Similarly, doping by Fe in the alloy (Ni$_{45.3}$Fe$_{5.3}$)Mn$_{23.8}$Ga$_{25.6}$ stabilized the austenitic phase down to 10 K.

The highest temperature of martensitic transformation $T_m = 571$ K was achieved for the Ni$_{50.0}$Mn$_{25.4}$Ga$_{20.3}$Ni$_{4.3}$ alloy. However, this doping also resulted in a significant reduction in Curie temperature to 325 K.

From the obtained experimental data, it is clear that to broaden the interval, where the MSM effect occurs, is impossible by single element doping within this substitutional range.
The well-established parameter $e/a$ was compared to the $N_e/a$ parameter. Martensitic transformation temperatures increase with increasing $e/a$ and $N_e/a$ parameters, with the latter providing a better linear fit and predicting the disappearance of martensitic transformation in the Fe-doped alloy.

The Curie temperature consistently increases in Fe-doped alloys and decreases in Ni-doped alloys. Co-doped alloys exhibit either an increase or a decrease in $T_C$ depending on the element that is substituted for. There is no significant correlation between Curie temperature and $e/a$ or $N_e/a$ parameters.

The doping effect is different for each compositional site; therefore, it is necessary to substitute for all three positions to reveal the full potential of the dopant. We suggest that the deficiency of the original element may affect the transition temperatures more strongly than the incorporation of a new element itself, at least up to 5 at.%. Although the site preference of the dopant is difficult to obtain experimentally, the cascade substitution is discussed and related to experimental data.

Apart from the valuable insight into doping by transitional elements, we expect that this experimental work can be treated as an incentive for ab-initio calculation explaining our observed trends.

**Supplementary Materials:** The following are available online at https://www.mdpi.com/article/10.3390/met11060850/s1; Figures S1–S9: magnetization and thermomagnetic curves of all alloys; Figures S10 and S11: Curie and martensitic transformation temperatures with respect to alloy composition; Figure S12: Martensite transformation start temperature with respect to $e/a$ or $N_e/a$ parameters; Figure S13: Saturation magnetization with respect to $e/a$ or $N_e/a$ parameters; Figure S14: Summary of X-ray diffraction patterns for all alloys.

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**Abbreviations**
The following abbreviations are used in this manuscript:

- MSM magnetic shape memory
- MT martensitic transformation
- FM ferromagnetic
- AFM antiferromagnetic
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