Prima Facie Evidence against Spin-Two Higgs Impostors

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Abstract

The new particle \(X\) recently discovered by the ATLAS and CMS Collaborations is widely expected to have spin zero, but this remains to be determined. The leading alternative is that \(X\) has spin two, presumably with graviton-like couplings. We show that measurements of the \(X\) particle to pairs of vector bosons constrain such scenarios. In particular, a graviton-like Higgs impostor in scenarios with a warped extra dimension of AdS type is \textit{prima facie} excluded, principally because they predict too small a ratio between the \(X\) couplings to \(WW\) and \(ZZ\), compared with that to photons. The data also disfavour universal couplings to pairs of photons and gluons, which would be predicted in a large class of graviton-like models.

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1 Introduction and Summary

The ATLAS \cite{1} and CMS \cite{2} Collaborations have discovered a new particle $X$ with mass $\sim 125$ to 126 GeV during their searches for the Higgs boson at the LHC. Supporting evidence for $X$ production in association with massive vector bosons $V \equiv W, Z$ at the TeVatron has been provided by the CDF and D0 Collaborations \cite{3}. If it is indeed a/the Higgs boson of the Standard Model, the $X$ particle must have spin zero. Since it has been observed to decay into pairs of photons, we already know that the $X$ particle cannot have spin one, but spin two is still an open possibility at the time of writing.

In view of the importance of determining the ‘Higgs’ spin, and the strong presumption that it has spin zero, it is particularly important to take an unbiased, approach to its measurement. Indeed, there is an extensive literature on possible strategies to distinguish the spin-parity $J^P$ of the $X$ particle, based on the kinematic characteristics of its production and decays \cite{4,5}. Examples include correlations between the momenta of particles produced in $X$ decays into $\gamma\gamma$, $WW^*$ and $ZZ^*$, and the $V + X$ invariant mass when it is produced in association with a massive vector boson $V$ \cite{6}. It is generally expected that significant evidence on the possible spin of the $X$ particle will shortly be provided by analyses of the existing TeVatron and 2012 LHC data.

In this paper we explore the extent to which the available data on $X$ production and decay already provide prima facie evidence that it is not a spin-two particle with graviton-like couplings in the frameworks of some popular models \cite{7}. As we recall in Section 2, the couplings $c_{g,\gamma}$ of a Higgs impostor $X$ to gluon pairs and photon pairs must be equal in many models with a compactified extra dimension, and hence

$$\Gamma(X \to gg) = 8 \Gamma(X \to \gamma\gamma).$$  \hspace{1cm} (1)

This relation is completely different from the case of a Higgs-like spin-zero particle, for which the $Xgg$ and $X\gamma\gamma$ couplings are induced by loop diagrams, and $\Gamma(X \to gg) = \mathcal{O}(\alpha_s/\alpha_{EM})^2 \Gamma(X \to \gamma\gamma)$. Numerically, at the one-loop level for the Higgs boson $H$ in the Standard Model in the limit $m_H \ll 2m_t, 2m_W$ one has

$$\Gamma(H \to gg) \simeq 37 \Gamma(H \to \gamma\gamma).$$  \hspace{1cm} (2)

Various analyses have shown that the current data are compatible with the $X$ particle being a Standard Model Higgs boson \cite{8,9}, and in particular with (2).

\footnotetext{1}{The spirit of this analysis is similar to that of \cite{7}, where prima facie evidence was presented that the ‘Higgs’ particle is not a pseudoscalar.}
Here we argue that the present data on $X$ production and decay disfavour the graviton-like spin-two prediction \([1]\), providing some prima facie evidence against the spin-two hypothesis. However, some graviton-like spin-two interpretations of the $X$ particle encounter more serious problems. For example, in models with a warped fifth dimension of AdS type one expects the following hierarchy of couplings to the energy-momentum tensors of different particle species:

$$c_b \simeq c_t \gtrsim c_W \simeq c_Z = \mathcal{O}(35) \times (c_g = c_\gamma > c_u, c_d). \quad (3)$$

As we show later, the hierarchy between $c_{W,Z}$ and $c_{g,\gamma}$ predicted in \([3]\) is in strong tension with the available data, which indicate a much greater hierarchy.

In the rest of this paper, we first review in Section 2 the couplings of a graviton-like spin-two boson, emphasizing the model-independence of the prediction \([1]\) and discussing the motivations for the more model-dependent predictions \([3]\). We then discuss the current data in Section 3, and the problems they raise for the predictions \([1]\) and \([3]\). Finally, in Section 4 we summarize our conclusions and discuss the prospects for gaining further insight into the nature of the $X$ particle.

## 2 Spin-Two Boson Couplings to Standard Model Particles

It was pointed out in \([10]\) that dimension-four couplings of a massive spin-two particle to a pair of Standard Model particles are forbidden by Lorentz invariance and gauge symmetry. The flavour and CP symmetries of the Standard Model then imply that the leading dimension-five terms should be proportional to their energy-momentum tensors $T^i_{\mu\nu}$, so that the couplings take the forms

$$\mathcal{L}_{int} = - \frac{c_i}{M_{eff}} G^{\mu\nu}T^i_{\mu\nu}. \quad (4)$$

In scenarios with extra dimensions, $M_{eff} \simeq \mathcal{O}(\text{TeV})$ is the effective Planck mass, whereas in composite models $M_{eff}$ would be a scale related to confinement. These two scenarios are, in general, related by some suitable extension of the AdS/CFT correspondence, and we consider here the formulation in terms of an extra dimension.

We consider general warped geometries of the form

$$ds^2 = w^2(z) (\eta_{\mu\nu}dx^\mu dx^\nu - dz^2), \quad (5)$$

where $w(z) = 1$ for a flat extra dimension, and in the case of warping à la AdS one has $w(z) = z_{UV}/z$. In general, $w(z)$ is a positive constant or decreasing function of $z$. 


In such a scenario, the Kaluza-Klein (KK) decomposition for spin-one particles leads to an equation of motion for the wave-function of the $n$th KK mode, $f_n(z)$, of the following form [11]:
\[ \partial_z (w(z) \partial_z f_n(z)) = -m_n^2 w(z) f_n(z). \] (6)

If the four-dimensional gauge symmetry is preserved by the compactification, as is the case for the SU(3) of QCD and the U(1) of electromagnetism, then the spin-one field has a massless zero mode, i.e., the lowest-lying KK mode has $m_0 = 0$, implying
\[ w(z) \partial_z f_0(z) = \text{constant}. \] (7)

Taking into account the Neumann boundary conditions on the boundary branes, there is only one solution, namely
\[ f_0(z) = C, \] (8)
where the constant $C$ is determined by requiring the canonical normalization for the four-dimensional gauge field.

Obviously, the graviton is not the source of electroweak symmetry breaking (EWSB). Instead, one may think that EWSB is triggered by a condensate of new fermions induced by new strongly-interacting gauge fields, as in technicolor models [12], a heavy Higgs, or, in the language of models with extra dimensions, by boundary conditions [13]. The graviton would couple to this source of EWSB, which we can parametrize by a field $\Sigma$ that could be spurious or dynamical and satisfies $\langle \Sigma \rangle = v$. In view of the small values of the $T$ and $\Delta \rho$ parameters [14], the field $\Sigma$ should respect an approximate custodial symmetry, and couple to the graviton via an effective interaction of the form
\[ \frac{c_{\Sigma}}{M_{\text{eff}}} G_{\mu\nu} D^\mu \Sigma D^\nu \Sigma, \] (9)

where
\[ D^\mu \equiv \partial^\mu + ig W^\mu + ig B^\mu. \] (10)

Gauge invariance implies that the graviton couples to the gauge eigenstates $W^a$ universally in [4], i.e., $c_W = c_Z$ as $g' \to 0$. Once EWSB occurs, the graviton would feel the effect through couplings induced via (10), which also respect custodial symmetry.

The next issue is the relation between $c_{\gamma,g}$ and $c_{W,Z}$. If it is assumed that electroweak symmetry is broken by boundary conditions on the IR brane, the support of the wave-functions of the transverse components of the $W$ and $Z$ is suppressed near this brane, so
that $c_{W,Z} < c_{g,\gamma}$. However, the wave-functions of the longitudinal components of the $W$ and $Z$ are localized near the IR brane, as are the wave-functions of the massive fermions $b$ and $t$, so that $c_{W_L,Z_L,b,t} > c_{g,\gamma}$. On the other hand, the wave-functions of light fermions such as the $u$ and $d$ are expected to be concentrated closer to the UV brane, so that $c_{u,d} \ll c_{g,\gamma}$.

One can estimate the hierarchy between $c_{\gamma,g}$ and $c_{W,Z}$ by accounting for the suppression due to the difference between localization on the IR brane, where the graviton has most of its support, and delocalization in the bulk. The couplings of the massive graviton to the massless gauge bosons, i.e., the gluons and photon, are suppressed by the effective volume of the extra dimension, namely

$$c_{\gamma,g} \simeq 1/\int_{z_{UV}}^{z_{IR}} w(z)dz,$$

and are therefore universal, leading to the result (1). If the extra dimension is of AdS type, $w(z) = 1/kz$, and the suppression is by a factor $\log M_{Pl}/TeV \simeq 35$. In other metrics, one could get a different degree of suppression. For example, one could introduce deviations from conformal invariance in AdS (or condensates of canonical dimension $d$ in the dual picture), by introducing metrics of the form

$$w(z) = 1/kz \left(1 + c_d \left(\frac{z}{z_{IR}}\right)^{2d}\right).$$

Those effects would not change the AdS result

$$c_{W,Z}/c_{\gamma,g} \lesssim \mathcal{O}(35)$$

by more than a factor $\mathcal{O}(1)$. On the other hand, one could obtain a larger difference by postulating a metric that is not asymptotically AdS.

In the dual picture, metrics of the form correspond to theories which become scale-invariant at high energies. This is a very attractive feature of a strongly-coupled theory, as one can relate low-energy quantities to the UV behaviour by using, for example, the operator product expansion. Therefore, $c_{W,Z}/c_{\gamma,g} \gg 35$ would mean that the composite theory does not have such behaviour in the UV, implying a loss of predictivity.

This derivation was made assuming that QCD and electromagnetism are present in the bulk. As an alternative, one could imagine localizing electromagnetism and strong interactions on a brane located at $z_\ast \in (z_{UV},z_{IR})$, in which case

$$c_{g,\gamma} \simeq \frac{w(z_{IR})}{w(z_\ast)}.$$
leading again to the relation (1). One could also imagine a situation where the gluon (or the photon) is stuck on a brane and the photon (or gluon) is in the bulk or on the opposite brane. However, this option is phenomenologically very disfavoured, since quarks are charged under both gauge groups and would need a non-negligible overlap with both fields, possibly leading to a large five-dimensional gauge coupling $g_{5D}$, implying a low cutoff of the effective theory $\Lambda_{NDA}$ as $\Lambda_{NDA} \propto 1/g_{5D}^2$. Also note that in the dual picture, the spin-two resonance could be made up of states with no color or no electric charge and this would invalidate the relation between decays to photons and gluons.

Localized kinetic terms do not modify this relation for massless gauge fields, since they modify only the right-hand side of the equation of motion (6), which is proportional to the mass. In the case of a massless zero mode, the effect is on the normalization of the mode in the bulk, namely the relation between the five-dimensional gauge couplings $g_5$ and their four-dimensional equivalents. However, this effect is absorbed by fixing the four-dimensional couplings of the zero-mode gauge fields to the Standard Model values and re-scaling the KK couplings. Since the graviton decays to photons and gluons depend only on the number of degrees of freedom, the relation (1) is unchanged.

To summarize, graviton-like couplings satisfy the following properties

- Due to current conservation: $c_g = c_\gamma$,
- Custodial symmetry: $c_W = c_Z$,
- For the theory to be asymptotically scale-invariant: $c_{W,Z} \lesssim \mathcal{O}(35)c_{\gamma,g}$,

which we exploit in the next Section of this paper.

Before closing this Section, however, we should mention one observation that disfavours a graviton-like explanation for the ‘Higgs’. The observed state is very light, with a mass $\simeq 125$ GeV whereas, if the graviton is a manifestation of extra dimensions, one would expect that the mass of the massive graviton would be given by

$$m_G \sim 1/z_{IR}.$$  \hspace{1cm} (15)

As other fields also live in the extra dimension, one would also expect comparatively light excitations of these fields, with masses typically of the order of $1/z_{IR} \simeq m_h$. For example, in the minimal AdS case $m_{s=2} \simeq 1.5m_{s=1}$, which is clearly ruled out by direct constraints. For example, a $Z'$ resonance with mass of order 100 GeV and electroweak couplings is ruled out by TeVatron and LHC searches $[19]$. On the dual side, one would argue along the same lines, but with $1/z_{IR}$ being replaced by the scale of confinement. In a QCD-like theory, one
would expect the masses of the resonances to increase with the spin, so that the lightest tensor meson would be heavier than the vector analogue of the $\rho$ meson. One might hope for a separation between the spin-two and spin-one excitations in metrics of more general form than AdS, but this is not the case. Using the techniques in Ref. [11], one can show that

$$m_{s=2}^2 \simeq \int dw(z)^{2s-1} \int dy/w(y)^{2s-1},$$

(16)

where $s$ is the spin. As $w(z)$ is a decreasing function, this leads to the conclusion that $m_{s=2} > m_{s=1}$.

Despite this objection, we consider the spin-two interpretation of the $X$ particle with an open mind, guided by the expectations (3).

3 Interpretation of Experimental Measurements

A generic experimental measurement of the number of $X$ particle events in any specific channel is proportional to a quantity of the form $\Gamma_i/\Gamma_{\text{Tot}}$, where $\Gamma_f$ is the decay rate into the observed final state, $\Gamma_{\text{Tot}}$ is the total decay rate, and $\Gamma_i$ is the rate at which the $X$ particle decays into the pair of partons that produce it. In the Standard Model, the dominant production process is $gg \to X$ and $\Gamma_i$ represents the decay rate for $X \to gg$\footnote{There are important QCD radiative corrections in both the production cross section and the $gg$ decay rate, but these are similar in magnitude, so their net effects are not important for our purposes. There are no such corrections in the graviton-like spin-two case, since it couples to the energy-momentum tensor.} though this should not be taken for granted in graviton-like models, as we discuss below. In the case of 'Higgs'-strahlung in association with a vector boson $V = W$ or $Z$, or of vector-boson fusion (VBF), $\Gamma_i$ represents the decay rate for $X \to VV^*$. In the Standard Model, processes with initial-state $\bar{b}b$ are negligible, in particular, because of the small density of $b$ partons in the incident protons, but this also needs to be reviewed in graviton-like models in view of the possibility that $c_b$ is enhanced as in (3). Likewise, processes with $\bar{t}t$ in the final state are known to contribute $\lesssim 0.5\%$ of Higgs production in the Standard Model, but could be more important in the graviton-like case. On the other hand, we can neglect processes with initial-state $\bar{u}u$ and $\bar{d}d$ because their couplings to the $X$ particle are expected to be very small in both the Higgs and graviton scenarios.

We first consider the experimental constraints on the ratios $\Gamma_\gamma/\Gamma_W$ and $\Gamma_\gamma/\Gamma_Z$. Information on $\Gamma_\gamma/\Gamma_{W,Z}$ is provided by data on the $X$ branching ratios, with only mild assumptions on the $X$ production mechanism(s) and spin. Concretely, we may write

$$\left| \frac{\Gamma_\gamma}{\Gamma_W} \right|_2 = \frac{K_\gamma}{K_W} \left| \frac{\Gamma_\gamma}{\Gamma_W} \right|_0,$$

(17)
and similarly for the $Z$ case, where the notation $|_s$ denotes the spin hypothesis under which the decay modes are analyzed, and the factors $K_f$ encode the differences in the kinematic acceptances for spin-two and spin-zero $X \to \gamma\gamma, WW^*$. Based on [5], we estimate that $K_\gamma \simeq 1$ (reflecting the large angular acceptances of ATLAS and CMS for the $\gamma\gamma$ final state) whereas $K_W \simeq 1.9$ (reflecting the fact that the ATLAS and CMS $WW^*$ analyses were optimized for the spin-zero hypothesis and have lower efficiencies in the spin-2 case), so that

$$\frac{\Gamma_\gamma}{\Gamma_W}|_2 = \frac{1}{1.9} \frac{\Gamma_\gamma}{\Gamma_W}|_0.$$  

The ratio $\Gamma_\gamma/\Gamma_W|_0$ may be parametrized in the form

$$\frac{\Gamma_\gamma}{\Gamma_W}|_0 = \mu_{LHC}^{gg\to h\to \gamma\gamma} \times \frac{\Gamma_\gamma}{\Gamma_W}|_{SM},$$  

where the signal strength factors $\mu_{LHC}^{f}$ are determined experimentally to be [3]

$$\mu_{gg\to h\to \gamma\gamma} = 1.54 \pm 0.28,$$

$$\mu_{gg\to h\to WW} = 0.83 \pm 0.29.$$ 

We conclude that

$$\frac{\Gamma_\gamma}{\Gamma_W}|_2 = (0.98 \pm 0.38) \times \frac{\Gamma_\gamma}{\Gamma_W}|_{SM}.$$ 

In the case of the $ZZ^*$ final state, we combine the ATLAS result with the CMS result obtained without applying the MELA analysis [2], obtaining

$$\mu_{gg\to h\to ZZ} = 0.91 \pm 0.25.$$ 

Since we do not use the MELA analysis, there is no efficiency correction analogous to [18], so we conclude also that

$$\frac{\Gamma_\gamma}{\Gamma_Z}|_2 = (0.91 \pm 0.25) \times \frac{\Gamma_\gamma}{\Gamma_Z}|_{SM}.$$ 

We have used MadGraph5 [20] to evaluate the decay rates for graviton-like $X \to WW^*$ and $ZZ^*$ decay as functions of $c_{W,Z}/M_{eff}$ [4] and compared them with standard calculations of graviton-like $X \to \gamma\gamma$ decay. Using a numerical computation, we estimate that

$$\frac{\Gamma_\gamma}{\Gamma_W}|_{Graviton} \simeq 280 \left( \frac{c_\gamma}{c_W} \right)^2,$$

$$\frac{\Gamma_\gamma}{\Gamma_Z}|_{Graviton} \simeq 2900 \left( \frac{c_\gamma}{c_Z} \right)^2.$$ 

It is well-known that the measured values of $\Gamma_\gamma/\Gamma_W$ and $\Gamma_\gamma/\Gamma_Z$ are somewhat higher than expected in the Standard Model, due to the apparent enhancement of $X \to \gamma\gamma$ events, but this does not have a big effect on our analysis.
Using (26), and the Standard Model values $\Gamma_\gamma/\Gamma_W|_{SM} = 0.0106$ and $\Gamma_\gamma/\Gamma_Z|_{SM} = 0.086$, we find that the result (22) corresponds to
\[
\frac{c_\gamma}{c_W} = 0.0061 \pm 0.0012, \\
\frac{c_\gamma}{c_Z} = 0.0071 \pm 0.0012, 
\] (27)
which are consistent with custodial symmetry:
\[
\lambda \equiv \frac{c_W}{c_Z} = 1.16 \pm 0.30, 
\] (28)
as already shown in [5]. Fig. 1 compares the constraint (28) on the possible deviation of $\lambda \equiv c_W/c_Z$ from custodial symmetry in the spin-two case (solid line) with the corresponding ratio $a_W/a_Z$ in the spin-zero case (dashed line), as shown in Fig. 15 of [5]. We see that, though the spin-zero case gives a marginally better fit to the data, there is currently no significant preference over the spin two option.

On the other hand, combining the results (27), we infer that
\[
c_V = (175 \pm 25) \times c_\gamma. 
\] (29)
Qualitatively, this result is $\gg 1$, as is the graviton-like spin-two expectation \[3\]. However, quantitatively the hierarchy \[29\] is much larger than the ratio $\mathcal{O}(35)$ expected in AdS warped compactifications. These models are disfavoured by well over $3\sigma$ and, as argued in Section 2, a larger value would be a sign of a theory which is not scale invariant in the UV.

In order to test whether $c_g = c_\gamma$, we consider the ratio of the rates for $gg \to X \to \gamma\gamma$ and $VBF \to X \to \gamma\gamma$, which is related to $\Gamma_g/\Gamma_W$:

$$\frac{\Gamma_g}{\Gamma_W} = F_{0.2} \frac{\left[ \frac{\Gamma_g \Gamma_\gamma}{\Gamma_{\text{Tot}}} \right]_{gg \to h \to \gamma\gamma}^{\text{LHC}}}{\left[ \frac{\Gamma_W \Gamma_\gamma}{\Gamma_{\text{Tot}}} \right]_{VBF \to h \to \gamma\gamma}^{\text{LHC}}} ,$$

where $F_{0.2}$ are the ratios of initial flux factors, kinematic factors, efficiency factors, etc. appearing in the measured rates for the $gg$- and VBF-induced cross sections under the spin-zero and graviton-like spin-two hypotheses, respectively. Assuming that these factors are similar (differences by $\mathcal{O}(1)$ are unimportant), we may write

$$\frac{\Gamma_g}{\Gamma_W}_{\text{measured}} / \frac{\Gamma_g}{\Gamma_W}_{\text{SM}} = \frac{\left[ \frac{\Gamma_g \Gamma_\gamma}{\Gamma_{\text{Tot}}} \right]_{gg \to h \to \gamma\gamma}^{\text{LHC}}_{\text{measured}}}{\left[ \frac{\Gamma_g \Gamma_\gamma}{\Gamma_{\text{Tot}}} \right]_{gg \to h \to \gamma\gamma}^{\text{LHC}}_{\text{SM}}} \times \frac{\left[ \frac{\Gamma_W \Gamma_\gamma}{\Gamma_{\text{Tot}}} \right]_{VBF \to h \to \gamma\gamma}^{\text{LHC}}_{\text{measured}}}{\left[ \frac{\Gamma_W \Gamma_\gamma}{\Gamma_{\text{Tot}}} \right]_{VBF \to h \to \gamma\gamma}^{\text{LHC}}_{\text{SM}}} ,$$

In order to evaluate this ratio, we use the parametrizations:

$$\left[ \frac{\Gamma_g \Gamma_\gamma}{\Gamma_{\text{Tot}}} \right]_{gg \to h \to \gamma\gamma}^{\text{LHC}}_{\text{measured}} = \mu_{gg \to h \to \gamma\gamma}^{\text{LHC}} \times \left[ \frac{\Gamma_g \Gamma_\gamma}{\Gamma_{\text{Tot}}} \right]_{gg \to h \to \gamma\gamma}^{\text{LHC}}_{\text{SM}} ,$$

$$\left[ \frac{\Gamma_W \Gamma_\gamma}{\Gamma_{\text{Tot}}} \right]_{VBF \to h \to \gamma\gamma}^{\text{LHC}}_{\text{measured}} = \mu_{VBF \to h \to \gamma\gamma}^{\text{LHC}} \times \left[ \frac{\Gamma_W \Gamma_\gamma}{\Gamma_{\text{Tot}}} \right]_{VBF \to h \to \gamma\gamma}^{\text{LHC}}_{\text{SM}} ,$$

and the following experimental values for the signal strength factors $\mu_i^{\text{LHC}}$:

$$\mu_{gg \to h \to \gamma\gamma}^{\text{LHC}} = 1.54 \pm 0.28 ,$$

$$\mu_{VBF \to h \to \gamma\gamma}^{\text{LHC}} = 1.98 \pm 0.84 ,$$

with the result

$$\frac{\Gamma_g}{\Gamma_W}_{\text{measured}} = (0.78 \pm 0.36) \times \frac{\Gamma_g}{\Gamma_W}_{\text{SM}} .$$

where $\Gamma_g/\Gamma_W|_{\text{SM}} = 0.40 \ (0.36)$ for $M_h = 125 \ (126)$ GeV. We also recall the Standard Model prediction $\Gamma_g/\Gamma_\gamma|_{\text{SM}} = 37$ for either value of $M_h$. Combining this with \[35\] and \[22\], we obtain the estimate

$$\frac{\Gamma_g}{\Gamma_\gamma}_{\text{measured,2}} \simeq 29 \pm 13 ,$$
where we have emphasized that this estimate applies to a spin-two graviton-like particle. This estimate is to be compared with the prediction of graviton-like models:

\[
\frac{\Gamma_g}{\Gamma_W} \bigg|_{\text{Graviton}} = 8 \frac{\Gamma_\gamma}{\Gamma_W} \bigg|_{\text{Graviton}},
\]

which, we recall, is not subject to radiative corrections because the coupling is proportional to the energy-momentum tensor. There is clearly some tension between the data (36) and the prediction (37) of the graviton-like model.

This discrepancy may be phrased in terms of the coefficient \( c_g \) using (37) in conjunction with the calculation (25):

\[
\frac{\Gamma_g}{\Gamma_W} \bigg|_{\text{Graviton}} \approx 2200 \left( \frac{c_g}{c_W} \right)^2 .
\]

Putting (35) and (38) together, we find

\[
\frac{c_g}{c_W} \approx 0.012 \pm 0.0027 .
\]

Combining with (27), we infer that

\[
c_g = (1.97 \pm 0.59) \times c_\gamma ,
\]

in poor agreement with the graviton-like spin-two expectation (3).

The above results for graviton-like models are displayed in the left panel of Fig. 2, which displays the correlation between the current experimental constraints on \( c_V/c_\gamma \) (horizontal axis) and \( c_g/c_\gamma \) (vertical axis). We see that the best fit corresponds to \( c_W/c_\gamma \sim 175 \) as shown in (29) and \( c_g/c_\gamma \sim 2 \) as shown in (40). We also see a tendency for smaller values of \( c_W/c_\gamma \) to be correlated with smaller values of \( c_g/c_\gamma \). However, we also see that the predictions \( (c_W/c_\gamma, c_g/c_\gamma) \sim (35, 1) \) of a graviton-like spin-two particle in warped space-time are jointly disfavoured by \( \gg 3\sigma \). In contrast, we see in the right panel of Fig. 2 that a global fit to all the available data under the spin-zero hypothesis is very compatible not only with the couplings to massive vector bosons having the Standard Model values (assuming custodial symmetry \( a_W = a_Z \)), but also the triangle diagrams responsible for the couplings of a spin-zero particle to \( gg \) and \( \gamma\gamma \). Defining \( A_{\gamma,g} \) to be the ratios of these triangle diagrams to their values in the Standard Model, we see that the data are very compatible with them having a common value \( A \equiv A_\gamma = A_g \) close to unity.

However, there is a potential loophole in the discussion of \( c_g \). As recorded in (3), the coupling of a graviton-like spin-two particle to \( \bar{b}b \) could be enhanced. One may ask whether an enhanced \( X\bar{b}b \) coupling could lead to \( X \) production processes involving \( b \) quarks becoming
Figure 2:  Left panel: the correlation between the values of $c_W/c_\gamma$ (horizontal axis) and $c_g/c_\gamma$ (vertical axis) found in a global fit to the current experimental data under the spin-two hypothesis. Right panel: a global fit under the spin-zero hypothesis to the couplings to massive vector bosons (assuming custodial symmetry and a common ratio to the Standard Model values) and to massless vector bosons $g, \gamma$ (assuming a common ratio $A \equiv A_g = A_\gamma$ to the values of the loop diagrams in the Standard Model).

sufficiently important to invalidate the above argument. In particular, one should consider the possibility that they could contribute to the event categories assumed by the ATLAS and CMS experiments to be due to $gg$ collisions, in which case (35) would become an upper limit and, accordingly, (36, 29) might be brought into agreement with the universality prediction of the graviton-like model.

In the Standard Model, the parton-level cross section for $gg \rightarrow H$ is a factor $\sim 50$ smaller than the parton-level cross section for $\bar{b}b \rightarrow H$ in the four-flavour renormalization scheme. Nevertheless, the total $gg \rightarrow H$ cross section ($\simeq 15$ pb at 7 TeV, see Table 1 of [21]) is much larger than the total $\bar{b}b$-related cross section as calculated in either the four- or five-flavour scheme ($\simeq 250$ pb, see Figs. 22 and 23 of [21]). This is because the $gg$ parton collision luminosity factor is much larger than the corresponding factor for $\bar{b}b$ collisions. In order to rescue the hypothesis that $c_g = c_\gamma$ in the graviton-like spin-two model, one would need the total $\bar{b}b$-related cross section to exceed total $gg \rightarrow H$ cross section by a factor $\sim 3$, which would require $c_b/c_\gamma \simeq 100$.

Such an enhancement is consistent, a priori, with the generic expectations (3), and could be probed experimentally by studying whether many $\bar{b}b$ pairs are produced in association with the $X$ boson. However, it would lead to suppressions of the branching ratios for the decay modes $X \rightarrow \gamma\gamma, WW^*$ and $ZZ^*$. On the other hand, the Fermilab observation of $X$ production in association with $W, Z$ implies that the decay rates for the decays $X \rightarrow WW^*$ and $ZZ^*$ must be similar to their Standard Model values and hence, by extension, also the
decay rate for $X \rightarrow \gamma \gamma$. Thus, the total $X$ decay width should be enhanced relative to its Standard Model value by a factor $\sim \frac{10^4}{(0.61/2 \times 10^{-3})} \sim 30$, so that $\Gamma_{\text{Tot}} \sim 100$ MeV: this is not inconsistent with the data.

As also seen in (3), one would expect that $c_t \gtrsim c_b$, with custodial symmetry suggesting that $c_t \simeq c_b$. In this case, one would have $c_t/c_W \sim 100 \times (c_\gamma/c_W) \simeq 0.6$. In this case, in the absence of a detailed calculation, one would expect the total $\bar{t}tX$ cross section to be smaller than in the Standard Model. We note that CMS and ATLAS have currently established upper limits on this cross section that are 4.6 and 13.1 times larger than the Standard Model prediction, respectively \cite{22}, under the assumption that the $X$ particle has spin zero. These upper limits need to be recalculated for the spin-two case, but there is no \textit{prima facie} contradiction with the possibility that $c_b/c_\gamma \simeq c_t/c_\gamma \simeq 100$.

4 Summary

We have shown that the available data on $X$ production and decay already disfavour the possibility that it is a spin-two impostor. It has been argued previously that such impostors should have graviton-like couplings to other particles, and one expects $c_g = c_\gamma$ in all such scenarios. In the favoured warped compactifications of AdS type, one also expects custodial symmetry so that $c_W = c_Z \equiv c_V$, and that $c_V/c_\gamma \simeq 35$. We have shown that, whereas $c_W = c_V$ is compatible with the data, they favour $c_g > c_\gamma$ and $c_V/c_\gamma \gg 35$. This last result is the strongest element in our \textit{prima facie} case against the $X$ particle being a spin-two Higgs impostor.

The advent of more data from the LHC 2012 run and more refined analyses of the Tevatron data will enable our arguments to be sharpened. We also expect that the LHC and Tevatron experiments will come forward with other, more direct, information about the spin of the $X$ particle. Probably nobody, least of all the authors, seriously expects that the $X$ particle has spin two. Nevertheless, this is the only available ‘straw person’ with which to compare the spin-zero expectation, in the same spirit as the angular distribution of three-jet events in $e^+e^-$ annihilation were calculated long ago for the (unexpected) scalar gluon case \cite{23}, to be compared with the distribution for the (confidently expected) vector gluon case. That comparison subsequently provided the first experimental verification that gluons indeed have spin one \cite{24}, confirming the theoretical expectation.

Theorists expect the contest between spin zero and spin two to be like a match between Brazil and Tonga\footnote{http://resonaances.blogspot.com/2012/10/higgs-new-deal.html}. The question is: what is the game - football (soccer) or rugby?
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