Negative Hall coefficients of heavily overdoped \( \text{La}_{2-x}\text{Sr}_x\text{CuO}_4 \)

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Abstract

The Hall coefficient \( R_H \) is investigated along the in-plane direction for carefully prepared \( \text{La}_{2-x}\text{Sr}_x\text{CuO}_4 \) thin films from \( x = 0.08 \) to \( x = 0.40 \). It is found that \( R_H \) becomes almost temperature independent around room temperature for \( x \geq 0.24 \), and its sign smoothly changes from positive to negative between \( x = 0.28 \) and \( 0.32 \), showing contrasting behavior to previously reported results. This result indicates that the carrier can be doped smoothly across the hole- to electron-dominant regions. According to the sign change of \( R_H \), superconductivity disappears for \( x \geq 0.32 \) films, which suggests that a positive \( R_H \) is one of the necessary conditions for superconductivity in \( p \)-type cuprates.

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Evolution of superconductivity according to carrier doping is an essential feature of high-temperature (high-$T_c$) cuprate superconductors. All high-$T_c$ cuprates have a two-dimensional square-lattice CuO$_2$ plane in common, on which an electronic ground state drastically changes from insulator to doped semiconductor, superconductor, and normal metal. One of the key concepts needed to reveal the mechanism of high-$T_c$ superconductivity is understanding how superconductivity occurs by carrier doping. For that purpose, people have started extensive studies on the carrier doping effect in the underdoped region soon after the discovery of high-$T_c$ cuprates. Due to an incredible amount of studies, we have now come to believe that a strong coupling among charge, spin, and lattice plays a significant role in the physical properties of underdoped cuprates, even though its direct relation to the occurrence of superconductivity is still veiled. On the other hand, physical properties of the overdoped metallic region have not been fully investigated mainly due to difficulty in preparing high-quality samples. Even for well-studied La$_{2-x}$Sr$_x$CuO$_4$ (LSCO), for example, it has been known that the oxygen deficiency becomes significant in the overdoped side, typically when $x$ exceeds 0.28. Thus, the experimental approach to superconductivity from the overdoped side using high-quality single crystals or thin films is limited only to two systems: LSCO and Tl$_2$Ba$_2$CuO$_{6+\delta}$ (Tl2201) and, because of the toxicity of Tl, LSCO has been and is still the most important compound for the study from the nonsuperconducting overdoped side.

It is still an open question whether or not heavily overdoped LSCO is really a normal Fermi liquid. Takagi et al. reported for $x = 0.34$ single-crystal thin films that in-plane resistivity ($\rho$) does not follow simple $T^2$ behavior but is well fitted by $T^{1.5}$. Nakamae et al. has recently found ideal $T^2$ resistivity behavior below $\sim 55$ K for $x = 0.30$ in a single crystal, but the resistivity at higher temperature region follows $T^{1.6}$ behavior. Similar temperature dependence has been reported for overdoped Tl2201 single crystals. The situation mentioned above means that there is a difficulty in judging whether or not heavily overdoped high-$T_c$ cuprates merge into a normal Fermi liquid only from a resistivity measurement.

The Hall coefficient ($R_H$) is a more robust parameter than resistivity, and is used to obtain direct information of carriers. However, the $R_H$ data for heavily overdoped LSCO has still been controversial. The first systematic study on the Hall effect of LSCO was done by Takagi et al. immediately after the discovery of high-$T_c$ cuprates. They reported for polycrystalline LSCO that $R_H$ possibly becomes negative at $x = 0.32$ and 0.34. However, they also described
in the same paper that an $x = 0.34$ single crystal shows a positive $R_H$. Such an unclear situation was reported also by Hwang et al.\(^7\) for polycrystalline sintered samples and single-crystal thin-film samples. They reported that the room-temperature $R_H$ becomes almost zero both for $x = 0.30$, and 0.34; $R_H$ does not obviously go to a negative side, but seems to stay around zero. Suzuki\(^8\) has reported the $R_H$ for LSCO thin films prepared by sputtering; he found that the $x = 0.36$ sample shows a positive $R_H$, which is clearly inconsistent with the above two results.\(^1,7\) These three results suggest the presence of two hurdles when we study the Hall effect of heavily overdoped LSCO. The first hurdle is that we must be very careful about the sample misalignment/orientation. In particular, we need to align the current direction perfectly parallel to the CuO\(_2\) plane, because even a slight misalignment may seriously influence the sign of Hall coefficients. As was demonstrated by Tamasaku et al.\(^9\) for the $x = 0.30$ crystal, $R_H$ is positive for $i \parallel$ CuO\(_2\) plane while it is negative for $i \perp$ CuO\(_2\) plane. Thus it becomes very important to minimize the misalignment between the CuO\(_2\) plane direction and the current path direction as much as possible, especially when the magnitude of $R_H$ is very small as in the overdoped samples. The other hurdle is the oxygen deficiency as was mentioned before.\(^2,10\) It is partially helpful to anneal the samples for a very long time under high-oxygen pressure.\(^2,3,4\) However, high-pressure annealing is not possible everywhere, and is hardly applicable to thin-film samples.

In this paper, we propose to solve these two problems by using epitaxial thin films combined with a strong oxidation technique, and carry out Hall-effect measurements to demonstrate that a sufficient amount of holes can be doped in LSCO at least up to $x=0.40$. We pay attention to the following two points in particular; a) whether $R_H$ indeed becomes negative above a certain $x$, or just stays at zero, and b) how the temperature dependence of $R_H$ goes with increasing $x$, or in other words, whether an ordinary Fermi liquid ($T$-independent $R_H$) indeed can be observed in the heavily overdoped LSCO.

All films were grown by a pulsed laser deposition (PLD) technique with low-pressure pure ozone as an oxidant.\(^11\) The films were all highly $c$-axis oriented as confirmed by x-ray diffraction. We used SrTiO\(_3\) (100) as a substrate in order to not only compare our data with several published data but also decrease the influence of a strong epitaxial-strain effect.\(^12\) It has been known that LSCO is highly susceptible to the lattice mismatch, and it is almost impossible to perfectly reproduce the transport properties of bulk crystals in thin-film samples.\(^13,14,15\) However, it has been experimentally shown\(^12\) that the epitaxial strain to
LSCO is not as large on SrTiO$_3$ (100) as on LaSrAlO$_4$ (001) and LSAT (100). We actually confirm that the effect of epitaxial strain is not killed completely even using SrTiO$_3$ (100), and the present films indeed have shorter $c$ axes than the bulk crystals have$^{16}$ for almost the entire $x$ range (Fig. III(b)), which indicates that finite tensile strain survives in our films. Substrate temperature during the deposition was set around 820 - 840°C, and the film thickness was kept around 1500 - 2500 Å. Samples are separated into two groups; the films for $x = 0.08$ - 0.22 were processed into a small six-terminal shape using photolithography and wet etching$^{17}$ while those for $x = 0.24$ - 0.40 were prepared using a metal mask (six terminal shape) in order to omit any post heat treatments. Ozone is indispensable for two reasons; first, we can keep the chemical composition of the films identical to the targets. It is known that in a usual PLD or sputtering technique that the excess Cu is necessary to be added in the target in order to compensate the Cu deficiency in the films.$^8$ However, this procedure makes the relation between Sr concentration and real hole density unclear and uncontrollable. Because the reduction of gas pressure can make the mean-free path of each ablated species longer than the target-substrate distance, the deviation of chemical composition is automatically suppressed as a result$^{18}$ We set the ozone pressure to 10 mPa during the film deposition, and increase it to 15 mPa during the cooling down procedure. Second, we can utilize a stronger oxidation ability of ozone than high-pressure oxygen. It is known that the activity of ozone at $T = 300$ K reaches $10^{19}$ times larger than that of oxygen,$^{19}$ implying an efficient compensation of oxygen deficiency. In the present case, we suppress the oxygen deficiency by supplying ozone until the film temperature decreases by $60$ - $65$°C. This procedure is applied for the sample with $0.20 \leq x \leq 0.40$. The other films with lower $x$ are annealed after the growth under the same conditions applied to bulk single crystals.$^{20}$

The temperature dependence of the in-plane resistivity of all the films is summarized in Fig. III(a). The figure shows a systematic change in magnitude and $T_c$. The magnitude of the resistivity in moderately doped films is slightly higher than that of bulk single crystals,$^{21}$ which is frequently observed when films are grown on SrTiO$_3$,$^{8,13,22}$ and considered to be one of the effects of the remanent epitaxial strain. The zero resistivity temperature ($T_{c0}$) is plotted as functions of $x$ in Fig. III(b), in which a conventional dome-shaped curvature is properly reproduced. The temperature dependence of Hall coefficients for these films are shown in Fig. III(c). In contrast to the resistivity data, $R_H$ shows better coincidence for $x \leq$
0.2 with those of bulk single crystals. \( R_H \) moderately increases towards low temperatures, shows a peak between 50 - 100 K, and rapidly decreases towards superconducting transition. The room temperature values are plotted in the inset of Fig. 8 which shows a smooth evolution of low-field \( R_H \) by Sr doping.

We focus on the heavily overdoped region in more detail. We again plot the resistivity and Hall data for \( x \geq 0.28 \) in Figs. 2(a) and (b). As is easily seen, superconductivity is clearly observed for \( x = 0.24 \) and 0.28, while zero resistivity is no longer observed for \( x \geq 0.32 \), which is consistent with Torrance et al. The transition width of \( x = 0.28 \) is far wider than that of \( x = 0.24 \), which indicates that the oxygen distribution becomes inhomogeneous with increasing \( x \). The onset of superconductivity observed in the \( x = 0.32 \) film may be caused also by the oxygen inhomogeneity. It is intriguing that the room-temperature \( R_H \) changes its sign in accordance with the disappearance of superconductivity. For \( x = 0.28 \), \( R_H \) keeps a very small but positive value of the order of \( 10^{-5} \) cm\(^3\)/C from 300 K to 200 K, and begins increasing towards the lower temperatures. The boundary between positive and negative \( R_H \) is found between \( x = 0.28 \) and 0.32. For \( x = 0.32 \), \( R_H(300K) \) is no longer positive but its temperature dependence looks similar to that of the \( x = 0.28 \) film, and also to that reported for \( x = 0.30 \) bulk single crystals. What is newly discovered is the \( R_H \) behavior of \( x = 0.36 \) and 0.40 films. For \( x = 0.36 \), \( R_H(300K) \) increases its magnitude to the negative side, is no longer positive down to \( T = 0 \) K, and \( dR_H/dT \) turns positive at room temperature suggesting that the high-temperature limit of \( R_H \) is much closer to zero. To our knowledge, these features have never been reported for LSCO. For \( x = 0.40 \), the low-temperature upturn behavior is no longer observed and \( R_H \) behaves as a typical metal. The doping dependence of \( R_H(T) \) behavior reminds us of the doping dependence of \( n \)-type cuprates (\( \text{Nd}_{2-x}\text{Ce}_x\text{CuO}_4 \) (NCCO) and (\( \text{Pr}_{2-x}\text{Ce}_x\text{CuO}_4 \) (PCCO)\(^{23,24,25} \) in which \( R_H \) changes its sign from negative to positive with increasing \( \text{Ce}^{4+} \) substitutions for \( \text{Nd}^{3+} \) or \( \text{Pr}^{3+} \). Therefore, the present data strongly indicates the similarity of electronic states between LSCO and NCCO (PCCO) at heavily overdoped regions.

It should be also noted that the occurrence of superconductivity and the sign change of \( R_H \) is not always correlated. We should remember that overdoped nonsuperconducting Tl2201 has a positive \( R_H \)\(^5 \) which is one of the counterevidences. Moreover, we have recently revealed that strong epitaxial strain can kill superconductivity completely at any doping region\(^{26} \) which also indicates that superconductivity can disappear even when \( R_H > 0 \). To
reveal how the epitaxial strain influences the sign of $R_H$ is our next subject.

Let us compare the present negative Hall coefficients with previously published data. Hwang et al.\textsuperscript{7} analyzed the temperature dependence of the Hall coefficient of LSCO with $0.15 \leq x \leq 0.34$ using a scaling function expressed as $R_H(T) = R_H^\infty + R_H^* f(T/T^*)$. In this manner, $R_H^\infty$ gives the value of the high-temperature $T$-independent part of $R_H$, and in our case $R_H(300 \text{ K})$ for $x \geq 0.24$ is a good approximation of $R_H^\infty$. Figure 3 shows the $x$ dependence of $R_H(300 \text{ K})$ of our films with $R_H^\infty$ shown in the inset of Fig. 2 of Ref. 7. In contrast to Hwang’s data, our $R_H(300 \text{ K})$ data shows no saturation even above $x = 0.30$; it keeps decreasing to a negative side while keeping the gradient, $dR_H/dx$, unchanged. This result strongly indicates that the carrier doping is done smoothly across the hole- to electron-dominant regions. It should be noted that this smooth sign change is consistent with the theoretical prediction by Shastry et al.,\textsuperscript{27} in which the $ac$ Hall coefficients were proposed to be a better measure of carrier concentration. If our $R_H$ around 300K can be regarded as an approximation of $ac$ Hall coefficients at a sufficiently high-frequency limit, our data looks consistent with these predictions in the following two points; 1) the sign change occurs at $x = 0.30 \sim 0.35$, and 2) the absence of saturating behavior at the sign-change concentration. The smooth sign change at similar Sr content was also predicted in a different theory constructed by Stanescu and Phillips,\textsuperscript{28} which again supports that the smooth sign change is a natural consequence of the $p$-type doping in LSCO.

Comparison with the results of ARPES measurements is also intriguing. Doping dependence of the Fermi surface in LSCO has been systematically investigated by Ino et al.\textsuperscript{29} According to them, the Fermi surface turned to an electron-like shape at $x = 0.30$, \textit{i.e.}, closed the Fermi surface around the $\Gamma$ point. The valence band clearly crosses the Fermi energy between the $(0,0)$ and $(\pi, 0)$ points (antinodal direction), and the Fermi surface approaches that of conventional metal. This is roughly consistent with the negative Hall coefficients in our films. One may wonder if the consistency between $R_H$ and ARPES data is invalid because the latest ARPES measurements by Yoshida et al.\textsuperscript{30} reveal that even at $x = 0.22$ the Fermi surface has a closed shape. However, we should remember that the sign of $R_H$ is not determined simply by a topology of the Fermi surface. It is widely known based on Ong’s argument\textsuperscript{31} that $R_H$ is mainly determined by the portion of the convex and concave parts of the Fermi surface, and the Fermi surface of the $x = 0.22$ crystal\textsuperscript{30} mostly consists of the convex part, which is consistent with positive $R_H$ at $x = 0.22$. Kontani et
calculated $R_H$ more rigorously. According to them, the vertex correction (back-flow process) should be taken into account when calculating $R_H$, and the portion of the Fermi surface inside and outside the magnetic Brillouin zone is important. Even according to their conclusion, ARPES data of the $x = 0.22$ single crystal looks consistent with positive $R_H$. One may suspect that the ARPES data was taken at $T = 20$ K, and hence it should be compared with the $R_H$ also at $T = 20$ K. However, we think that the low-temperature up-turn of $R_H$ is not a good measure of hole concentration, because it is strongly influenced by impurity scattering. To give an example, we show resistivity and Hall data for two different $x = 0.36$ films in Fig. 4(a). One can see that a lower resistivity sample (A) shows a stronger upturn in $R_H$ at low temperatures, while the magnitude of $R_H$ at room temperatures are insensitive to a difference of resistivity. Thus, we may regard the room-temperature $R_H$ as a more direct measure of carrier concentration.

After seeing the increase of $|R_H|$ to the negative side, we may reasonably understand the increase of resistivity when $x$ exceeds 0.32 to be intrinsic. In previous studies, the oxygen deficiency that becomes remarkable in heavily overdoped region is believed to be the main reason of this resistivity increase. The present result indicates that the Fermi surface starts to shrink once the doping exceeds $x \approx 0.3$, which leads to the decrease of in electron concentration. Thus, the resistivity may increase if the effective mass of electron is kept unchanged. It is interesting to perform an optical reflectivity measurement, with which we can estimate the density of the free carriers summed up to a finite frequency.

We briefly mention the temperature dependence of resistivity of the $x = 0.40$ film. Figure 2(b) suggests an absence of special Sr concentration at which $R_H$ strictly becomes temperature independent. However, the $R_H$ for $x = 0.40$ shows weaker temperature dependence than the others. Thus, it is meaningful to analyze the temperature dependence of the resistivity of this film. The result is shown in Fig. 4(b). We do not observe perfect $T^2$ behavior as similar to previous results. The temperature dependence is better expressed as $T^{1.5} \sim T^{1.6}$, which indicates the mixture of $T$ linear behavior with the $T^2$ one. We don’t know whether the further doping realizes pure $T^2$ behavior or not. However, the presence of $T$-linear term in $x = 0.40$, where $R_H$ becomes almost temperature independent, indicates that the electron-electron scattering is not the only scattering process even in heavily overdoped LSCO.

In summary, we measured the Hall coefficients of LSCO thin films grown under ozone
atmosphere, which effectively suppresses the oxygen deficiency. These films demonstrate a smooth change of the Hall coefficients from positive to negative at $T = 300K$, which shows a clear contrast to the previously reported results. The temperature dependence of Hall coefficients almost diminishes at $x = 0.40$ while the temperature dependence of resistivity still follows $T^{1.5} \sim T^{1.6}$. The sign change of $R_H$ is consistent with the shape of the Fermi surface determined by an ARPES measurement.

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FIG. 1: (color online). (a) Temperature dependence of $dc$ resistivity for $0.08 \leq x \leq 0.40$. (b) The line with red filled circles shows the $x$ dependence of $T_c$ (left axis). It shows a smooth change with $x$. The line with blue filled squares shows the $x$ dependence of the $c$-axis length which shows shorter values than those of bulk crystals (blue solid line) for $x \geq 0.12$. (c) Temperature dependence of $R_H$. The data were taken by sweeping the magnetic field between $\pm 1$ T for $0.08 \leq x \leq 0.22$, and $\pm 6$ T for $0.24 \leq x \leq 0.40$. 
FIG. 2: (color online). Close-up data of resistivity (a) and $R_H$ (b) for $x \geq 0.24$. 
FIG. 3: (color online). Plot of $R_H$ at 300K of the present work for $x \geq 0.24$ with $R_H^\infty$ from Ref. 7. Inset shows the $x$ dependence of $R_H$ at 300K for the entire doping range.
FIG. 4: (color online). (a) Temperature dependence of resistivity and Hall coefficients for the two $x = 0.36$ films. (b) $T^{1.5}$, $T^{1.6}$, and $T^2$ plots of the resistivity data for $x = 0.40$. 