EVOLUTION OF THE CRAB NEBULA IN A LOW ENERGY SUPERNova

HAIFENG YANG AND ROGER A. CHEVALIER

Department of Astronomy, University of Virginia, P.O. Box 400325, Charlottesville, VA 22904, USA; hy4px@virginia.edu, rac5x@virginia.edu

Received 2015 February 4; accepted 2015 May 10; published 2015 June 15

ABSTRACT

The nature of the supernova leading to the Crab Nebula has long been controversial because of the low energy that is present in the observed nebula. One possibility is that there is significant energy in extended fast material around the Crab but searches for such material have not led to detections. An electron capture supernova model can plausibly account for the low energy and the observed abundances in the Crab. Here, we examine the evolution of the Crab pulsar wind nebula inside a freely expanding supernova and find that the observed properties are most consistent with a low energy event. Both the velocity and radius of the shell material, and the amount of gas swept up by the pulsar wind point to a low explosion energy (∼1050 erg). We do not favor a model in which circumstellar interaction powers the supernova luminosity near maximum light because the required mass would limit the freely expanding ejecta.

Key words: ISM: individual objects (Crab Nebula) – supernovae: general – supernovae: individual (SN 1054)

1. INTRODUCTION

The identification of the supernova type of SN 1054, the event leading to the Crab Nebula, has been an enduring mystery. The amount of mass in the Crab filaments, 4.6 ± 1.8 M⊙ (Fesen et al. 1997), and their typical velocity, 1260 km s⁻¹ (Temim et al. 2006), imply a kinetic energy of ∼7 × 10⁵⁹ erg, considerably less than the ∼1 × 10⁶¹ erg inferred for typical core collapse supernovae. One possible reason for the discrepancy is that what we view as the Crab Nebula is only the inner region of a more extended supernova event, which has a normal energy, ∼10⁶¹ erg (Chevalier 1977). A constant density freely expanding region with this energy and mass of 6 M⊙ would extend to ∼5300 km s⁻¹. However, there is no sign of such a fast ejecta envelope interacting with the surrounding medium at X-ray (Seward et al. 2006) or radio wavelengths (Frail et al. 1995), which suggests that the density of the surrounding medium is low and the fast ejecta would be in free expansion. In that case, the freely expanding ejecta are heated and photoionized by the radiation from the Crab Nebula (Lundqvist et al. 1986; Wang et al. 2013), but they have not been clearly detected in either emission lines (Fesen et al. 1997) or in absorption to high velocities along the line of sight to the central pulsar (Sollerman et al. 2000; Lundqvist & Tziambtzis 2012; P. Lundqvist et al. 2015, in preparation).

If the surrounding ∼10⁶⁹ erg supernova remnant is absent, SN 1054 must have been a low energy and relatively low mass event, and there is theoretical support for such a view. Nomoto et al. (1982) found that the abundances in the Crab Nebula pointed to a progenitor mass in the range 8–10 M⊙ and a probable electron capture supernova. Models of electron capture supernovae have shown that neutrino driven explosions occur, but with a relatively small energy ≥1 × 10⁵⁶ erg (Kitaura et al. 2006). On the observational side, low energy (and low velocity) supernovae have been discovered, including IIP events such as SN 1997D, with an estimated energy of 10⁵⁶ erg (Chugai & Ulrich 2000). However, SN 1997D had a peak absolute magnitude of −14, considerably fainter than SN 1054 at maximum. Chugai & Ulrich (2000) suggested that SN 1054 was a low energy supernova, with the luminosity provided by circumstellar interaction. Smith (2013) noted that low velocity, Type IIb events like SN 1994 W and SN 2011ht are likely examples of such events and are potential analogs to SN 1054. However, Tominaga et al. (2013) followed the presupernova evolution as well as the explosion of an electron capture supernova, finding that a peak luminosity comparable to SN 1054 could be produced without strong circumstellar interaction; the high peak luminosity is related to the large extent of the progenitor star.

In the circumstellar interaction scenario for the peak emission from SN 1054, the dense filaments in the Crab contain circumstellar material and the medium around the observed nebulae is the initial surroundings, not supernova ejecta. An alternate view, which we investigate here, is that the nebula is surrounded by freely expanding ejecta, as in the model of Chevalier (1977), but we allow for a low energy supernova. Basic constraints on the model are discussed in Section 2. Pulsar wind bubble models are presented in Section 3 and the conclusions are in Section 4. The observations of the Crab are spread over the past decades. Here we take 1994 as a typical time of observation so that the age of the Crab Nebula is 940 years. The distance to the Crab is taken to be 2 kpc (Trimble 1973).

2. OBSERVATIONAL CONSTRAINTS

The view taken here is that the outer boundary of the observed Crab is the interface of the pulsar wind nebula with freely expanding ejecta to the outside, as in the model of Chevalier (1977). The fact that the synchrotron emitting nebula fills the region of thermal emission is highly suggestive of the outer boundary being the boundary with freely expanding ejecta. Additionally, Sankrit & Hester (1997) found that the emission of C IV and Ne V at the outer edge of the Crab is consistent with shock emission where the pulsar bubble is driving into freely expanding ejecta, but is inconsistent with a photoionization model. The Ne V emission, in particular, appears to come from a “skin” to the Crab (Hester 2008). The basic model presented by Sankrit & Hester (1997) has a shock velocity of vsh = 150 km s⁻¹ and a preshock density of ρ₀ = 12.7 m_H cm⁻³, where m_H is the proton mass. The model requires that there be a cooling shock wave to produce the line emission, although there may not be such a shock front around
the outer parts interact with the presupernova mass loss, while the inner parts interact with an expanding pulsar wind bubble.

3. EVOLUTION OF THE CRAB NEBULA

There are several components of the evolutionary model. In the presupernova stage, there is mass loss that provides the outer target for the expanding supernova. Within days after the supernova, the supernova ejecta approach free expansion. The outer parts interact with the presupernova mass loss, while the inner parts interact with an expanding pulsar wind bubble.

3.1. Approximate Model

Our aim is to examine the evolution of the Crab Nebula, considering the dependence on the supernova energy. We begin with the supernova explosion, which results in an inner flat and outer steep density profile. The ejecta are expected to reach free expansion within a few days and we approximate the profile by

\[
\rho = \begin{cases} 
  A r^{-3} & \text{for } V \leq V_f \\
  A r^{-3} \left( \frac{V}{V_f} \right)^{-7} & \text{for } V > V_f,
\end{cases}
\]  

(2)

where \( A \) is a constant, \( V = \frac{dr}{dt} \) is the velocity of freely expanding gas, and \( V_f \) is the transition velocity from a flat to a steep density profile. A comparison to the more accurate profile used in Section 3.3 is shown in Figure 2. The mass and energy of the supernova are given by \( M_{SN} = 7\pi A V_f^2/3 \) and \( E_{SN} = 7\pi A V_f^5/5 \),
so that $V_t = (5E_{SN}/3M_{SN})^{1/2} = 1.29 \times 10^7 E_5^{1/2} M_5^{-1/2} \text{ km s}^{-1}$, where $E_{50} = E_{SN}/(10^{50} \text{ erg})$ and $M_5 = M_{SN}/5 M_\odot$. Also, $A = 6.34 \times 10^{45} E_5^{3/2} M_5^{5/2} \text{ g s}^{-3}$.

On a timescale of 100s of years, the pulsar bubble expands into the freely expanding ejecta on the inside. For the Crab pulsar, we take a period $P = 0.0331$ s, $P = 4.2 \times 10^{-13}$ s s$^{-1}$, and a constant braking index $n = 2.5$ (Lyne et al. 1988). Using

$$P = P_0 \left(1 + \frac{t}{\tau}\right)^{n-1},$$

where $P_0$ is the initial period and $\tau$ is a constant timescale, and the above parameters, we find $\tau = 725$ years for $t = 940$ years. With a neutron star moment of inertia of $10^{45} \text{ g cm}^2$, the current spindown power is $\dot{E} = 4.6 \times 10^{39} \text{ erg s}^{-1}$ and it evolves as

$$\dot{E} = \dot{E}_0 \left(1 + \frac{t}{\tau}\right)^{-n+1}/n-1,$$

where $\dot{E}_0$ is the initial power. Assuming the observations were made at an age of 940 years, we have $\dot{E}_0 = 3.2 \times 10^{39} \text{ erg s}^{-1}$. The average power input up to time $t$ is

$$\dot{E}_a = \frac{(n-1)\dot{E}_0}{2t} \left[1 - \left(1 + \frac{t}{\tau}\right)^{-2n-1}\right].$$

For the Crab pulsar parameters, $\dot{E}_a = 0.39\dot{E}_0 = 1.2 \times 10^{39} \text{ erg s}^{-1}$ at the present time.

The expansion of the pulsar bubble is determined by the equations of conservation of mass, momentum, and energy (Chevalier 1977):

$$\frac{dM_{sw}}{dt} = 4\pi R^2 \rho (V_t - V),$$

$$M_{sw} \frac{d^2R}{dt^2} = 4\pi R^2 \left[P - \rho (V_t - V)^2\right].$$

The pulsar bubble initially expands in the constant density inner region of the ejecta. If the pulsar power can be regarded as constant, the expansion is self-similar and the bubble radius is (Chevalier 1977)

$$R = \left(\frac{875 V_t^3 \dot{E}_a}{396 M_{SN}}\right)^{1/5} t^{6/5}.$$  

This evolution implies that the time to sweep out the ejecta to velocity $V_t$ is

$$t_i = \frac{132 E_{SN}}{175 \dot{E}_a}.$$  

Taking $E_\dot{E}$ for the Crab pulsar, we have $t_i = 1940E_{50}$ years, so the shell is still primarily inside of the density inflection point. Equation (9) can be used to find the velocity of the shell at the present age of the Crab

$$V_t = \frac{6 R}{5 \tau} = 1.28 \times 10^3 E_{50}^{3/10} M_5^{-1/2} E_{a39}^{1/5} \text{ km s}^{-1}.$$  

The velocity is less than that at the outer edge of the Crab Nebula, but is comparable to that deduced from observations of bright filaments in the Crab. An important point is that a supernova energy of $10^{50}$ erg gives an outer velocity in approximate agreement with the Crab Nebula dense filaments, while $10^{51}$ erg gives too high a velocity.

In this model, the ratio of swept up to total ejecta mass is

$$\frac{M_{sw}}{M_{SN}} = 0.68 \left(\frac{\dot{E}_a}{E_{SN}}\right)^{3/5} = 0.33 E_{50}^{-0.6} E_{a39}^{0.6}$$

for the age of the Crab Nebula. This value is at the low end of what is allowed by estimates of the observed swept up mass and the mass of the progenitor star. Going to a supernova energy of $1 \times 10^{51}$ erg would decrease the predicted ratio by a factor of 4 to well below the observed value.

In this simple model, $V_t = (6/5)(R/t_a)$, so that

$$\Delta T = t_a - \frac{R}{V_t} = \frac{t_a}{6} = 157 \text{ years},$$

independent of other parameters. The result is larger than that deduced from optical observations. If there are the dependences $E \propto t^{-s}$ and central density $A \propto r^{-\delta}$, dimensional analysis shows that the $1/6$ factor in Equation (13) becomes $(1 - s + \delta)/(6 - s)$. The density is expected to drop with radius, giving larger acceleration and an increasing discrepancy between the theory and observation. The power input $\dot{E}$ is expected to drop with time, decreasing the acceleration and improving the discrepancy between the theory and observation. The more detailed model presented in Section 3.3 has the capability to give better agreement with the observations.
The density in the flat part of the supernova density profile at an age 940 years is \( \rho_f = 2.4 \times 10^{-23} M_{SN}^{0.2} E_{50}^{-0.3/2} \) g cm\(^{-3}\). If the free expansion velocity at the outer edge of the Crab is 1600 km s\(^{-1}\) as discussed above, the density at that point is 0.54 \( \times 10^{-23} \) g cm\(^{-3}\), which is somewhat below the preshock density of 2.1 \( \times 10^{-23} \) g cm\(^{-3}\) inferred by Sankrit & Hester (1997) in their radiative shock model. An energy of 1.6 \( \times 10^{50} \) erg would improve the agreement, but with an energy of 1 \( \times 10^{51} \) erg the highest ejecta density is 0.077 \( \times 10^{-23} \) g cm\(^{-3}\). The radiative shock model is more consistent with a low energy explosion. The observed shell is only partial, at lower shell velocities (Sankrit & Hester 2008), as would be expected for the density profile proposed here. We note that the outer edge is in the region of declining density here, whereas it is within this region in the discussion of the radial expansion because the outer edge of the Crab Nebula is substantially outside of the dense filaments. This issue is further considered in Section 3.3.

### 3.2. Interaction with Dense Mass Loss

In the SN IIn-P model of Smith (2013), the supernova interacts with dense circumstellar matter, with mass \( M_{CS} \), on a timescale of \( \sim 10^6 \) days. The interaction may be responsible for the optical light from the supernova near maximum. In the presence of the circumstellar material, the density profile in Equation (2) has a cut-off, at some velocity \( V_c \). All the material with speed higher than \( V_c \) interacts with circumstellar material and forms a dense shell with velocity \( V_c \). We initially assume that the pre-supernova velocity of the initial circumstellar material is negligible, compared to the supernova expansion. Under this assumption, the radial momentum of matter with velocity \( >V_c \) is \( P_r(V > V_c) = M(V > V_c) \times V_c \). Assuming \( V_c > V_t \), we find \( P_r(V > V_c) = M(V > V_c) \times 4V_t^3/3 \), leading to \( M(V > V_c) = 3M_{CS} \) after the circumstellar matter has been swept up. The total mass of the shell, including circumstellar and ejecta components, is \( M_{Shell} = 4M_{CS} \).

For \( V_c > V_t \) we find
\[
V_c = \left( \frac{M_{SN}}{7M_{CS}} \right)^{1/4} V_t, \tag{14}
\]
so the condition for \( V_c > V_t \) is \( M_{SN} > 7M_{CS} \). When \( V_c < V_t \), an integral shows that the relation is
\[
\frac{M_{CS}}{M_{SN}} = \left( \frac{V_c}{V_t} \right)^{-1} - 1 + \frac{1}{7} \left( \frac{V_c}{V_t} \right)^3. \tag{15}
\]
Values of \( M_{SN}/M_{CS} \) for various values of \( V_c/V_t \) are given in Table 1.

We have assumed here that the swept up shell of ejecta and circumstellar medium is thin because the internal energy generated by the interaction is carried away by radiation. This is a reasonable assumption in cases where the radiation is inferred to carry a significant part of the supernova energy (e.g., Chugai et al. 2004). The radiated energy is then
\[
E_{rad} = \Delta E = E_{SN} \left( V > V_c \right) - \frac{1}{2} M_{Shell} V_c^2, \tag{16}
\]
where \( E_{SN}(V > V_c) \) is the energy in the freely expanding ejecta with velocities \( >V_c \). If \( V_c > V_t \), we find
\[
E_{rad} = \frac{5}{21} E_{SN} \left( \frac{V_c}{V_t} \right)^{-2} = \frac{25 E_{SN}^2}{63 M_{SN}} V_t^{-2}, \tag{17}
\]
so that \( E_{rad} = 4.0 \times 10^{49} E_{SN} M_{SN}^{-1} V_{t,3}^3 \) erg, where \( V_{t,3} = V_t/1000 \) km s\(^{-1}\). The value of \( E_{rad} \) for SN 1054 is not well determined from the Chinese observations. The light curve is roughly consistent with a normal SN II, so that \( E_{rad} \approx (1-3) \times 10^{49} \) erg. Mauerhan et al. (2013) estimated a radiated energy of (2-3) \( \times 10^{49} \) erg for the Type IIn-P SN 2011ht. If \( V_c = V_t \), we have \( E_{rad} = 2.4 \times 10^{49} E_{50} \) erg, which suggests that \( V_c \) is close to \( V_t \) or 1.29 \( \times 10^4 \) km s\(^{-1}\) for the standard parameters. However, the profile of freely expanding gas is cut off at \( V_t \) and we argued in Section 2 that there is freely expanding gas over the velocity range 1600–2500 km s\(^{-1}\). The high velocity of free expansion suggests that \( V_c \) is at least twice \( V_t \), which drops \( E_{rad} \) by a factor of 4. There is thus a discrepancy between the Type IIn-P model for SN 1054 and the evidence for freely expanding ejecta in the Crab Nebula.

In the model of Tominga et al. (2013), the progenitor is a super asymptotic giant (SAGB) star with an estimated mass loss rate of \( 10^{-7} M_{\odot} \) yr\(^{-1}\) and a wind velocity of 29 km s\(^{-1}\). In their discussion of SN 1054 as an electron capture event, Moriya et al. (2014) took the SAGB wind velocity to be 10 km s\(^{-1}\). The wind duration is \( \sim 10^4 \) years, so it extends to (3–9) \( \times 10^{17} \) cm, or (0.1–0.3) pc in radius. Unlike the case of a Type IIn-P supernova, the forward shock wave is nonradiative from an early age, although the reverse shock is radiative while the interaction region is in the dense wind, for the standard parameters. For the supernova density profile given in Equation (2), the interaction shell moves through the wind on a timescale of 200 years. The velocity of freely expanding gas at that point is 1460 km s\(^{-1}\). In this case, the shocked gas adiabatically expands and cools after the shock wave has traversed the dense wind, and the gas is ultimately expected to return to free expansion. We do not examine the details of this process here, but note that energy conserving interaction with a wind appears not to be ruled out for the Crab.

### 3.3. Detailed Pulsar Nebula Model

In the previous sections, we assumed a simple form for the freely expanding supernova density profile as well as steady pulsar power input to enable analytic estimates of the model parameters. Here, we use a supernova density profile based on detailed calculations (Matzner & McKee 1999) and the standard evolution of the pulsar power (Equation (4)). The ordinary differential Equations (6)–(8) for the evolution of the pulsar bubble are solved with a Runge–Kutta scheme.

In previous discussions of pulsar nebula expansion in a supernova, the supernova has normal energy (\( 10^{51} \) erg) and the expansion of the nebula is just in the inner flat part of the

### Table 1

| \( V/V_t \) | \( M_{SN}/M_{CS} \) |
|----------|-----------------|
| 0.25     | 0.33            |
| 0.5      | 0.98            |
| 0.75     | 2.5             |
| 1.0      | 7.0             |
| 1.5      | 35              |
| 2.0      | 112             |
density profile. For a low energy supernova, the transition to the outer steeply dropping part of the profile may become important. The supernova density profile is shown in Figure 2 for an energy of $1 \times 10^{50}$ erg and an ejecta mass of $5 M_\odot$. The model is intended for a red supergiant progenitor star, as might be expected (Tominaga et al. 2013). The model of Matzner & McKee (1999) for red supergiants has a parameter $q$, which is related to the core-envelope mass ratio and is in the range 0.3–0.8; we choose $q = 0.5$. At small velocities, the profile approaches a flat power law with index $\delta = 0.21$ and at high velocities a steep power law with index $\rho = 11.7$ (Figure 2).

A problem with comparing the model to the actual Crab Nebula is that the model assumes that the pulsar bubble sweeps up a thin shell, while the Crab filaments are spread in radius, presumably as a result of the Rayleigh–Taylor instability. We consider two cases to cover the possibilities. In the first, the diameter of the Crab is taken to be 3.3 pc, consistent with the outer boundary of the Crab. Assuming that the filaments at the outer boundary have the typical $\Delta t = 75$ years, we have a velocity of 1840 km s$^{-1}$. For the other case, we assume that the velocity of the dense shell is characterized by that of the dense filaments, about 1260 km s$^{-1}$ (Temim et al. 2006). Now assuming that $\Delta t = 75$ years leads to a diameter of 2.23 pc. We expect that the two cases will bracket the actual Crab Nebula.

In order to estimate the goodness of fit of assumed models, we calculated

$$\chi^2 = \left[\frac{(R_{\text{fit}} - R_0)}{R_0}\right]^2 + \left[\frac{(V_{\text{fit}} - V_0)}{V_0}\right]^2$$  \hspace{1cm} (18)

where $R_{\text{fit}}$ and $V_{\text{fit}}$ are the estimated observed values of the shell radius and velocity, and $R_0$ and $V_0$ are the results of models for various values of ejecta mass $M_{\text{SN}}$ and supernova energy $E_{\text{SN}}$. In Figures 3 and 4, the darkness of the plots indicates the value of $\log(\chi^2)$. Figure 3 shows models with $R_{\text{fit}} = 1.65$ pc and $V_{\text{fit}} = 1840$ km s$^{-1}$, where the model parameters are the total ejecta mass, $M_{\text{SN}}$, and the supernova energy $E_{\text{SN}}$. If $M_{\text{SN}}$ is $6.6 \pm 1 M_\odot$, or less, as discussed in Section 2, the energy of the supernova is $E_{\text{SN}} \approx 1.0 \pm 0.5 \times 10^{50}$ erg. Figure 4 shows results for the assumption of the compact shell with $R_{\text{fit}} = 1.1$ pc and $V_{\text{fit}} = 1260$ km s$^{-1}$. The acceptable models occur at low energy with $E_{\text{SN}} \lesssim 0.5 \times 10^{50}$ erg.

Another constraint comes from the swept up mass in the shell, which is estimated as $4.6 \pm 1.8 M_\odot$ from the observations (Fesen et al. 1997). Figure 5 shows the swept up mass resulting from a given total ejecta mass, $M_{\text{SN}}$, and the supernova energy $E_{\text{SN}}$. With the limit on $M_{\text{SN}}$, a low value for the energy, $\lesssim 10^{50}$ erg, is indicated, in agreement with the approximate model described in Section 3.1. A recent estimate of the mass in the Crab filaments is $7.2 \pm 0.5 M_\odot$ (Owen & Barlow 2015); using this higher mass would yield an even stricter limit on the energy.
Also, the density profile of the freely expanding gas near the edge of the Crab Nebula (velocity \(\sim 1600 \text{ km s}^{-1}\)) has a density gradient between that of the outer steep power law and the inner flat region (Figure 2). This is in accordance with the findings of Sollerman et al. (2000) on the distribution of C IV outside the main nebula. A higher energy supernova would give a relatively flat density profile for the supernova ejecta just outside the main body of the Crab.

4. CONCLUSIONS

Independent lines of evidence support a low energy \(\sim 10^{50} \text{ erg}\) for the supernova giving rise to the Crab Nebula. The evidence includes the radius and acceleration of the Crab shell, the mass of swept up ejecta in the Crab shell, the presence of a radiative shock wave around part of the Crab shell, and the decreasing amount of C IV in the region surrounding the nebula.

The model proposed here combines the low energy supernova view of the Crab supernova with expansion into freely expanding gas. However, we do not consider the interaction of the freely expanding gas with its surroundings. The nature of the presupernova mass loss and the interaction of the supernova with the mass loss remains unclear. Further studies of the region around the Crab Nebula are warranted.

We are grateful to Robert Fesen, Peter Lundqvist, and the referee for useful comments on the manuscript. This research was supported in part by NASA grant NNX12AF90G.

REFERENCES

Bietenholz, M. F., Kronberg, P. P., Hogg, D. E., & Wilson, A. S. 1991, ApJL, 373, L59
Black, C. S., & Fesen, R. A. 2015, MNRAS, 447, 2540
Chevalier, R. A. 1977, in Supernovae, ed. D. N. Schramm (Dordrecht: Reidel), 53
Chugai, N. N., Blinnikov, S. I., Cumming, R. J., et al. 2004, MNRAS, 352, 1213
Chugai, N. N., & Utrobin, V. P. 2000, A&A, 354, 557
Clark, D. H., Mordin, P., Wood, R., et al. 1983, MNRAS, 204, 415
Fesen, R. A., Shull, J. M., & Harford, A. P. 1997, AJ, 113, 354
Frail, D. A., Kassim, N. E., Cornwell, T. J., & Goss, W. M. 1995, ApJL, 454, L129
Hester, J. J. 2008, ARA&A, 46, 127
Kitaura, F. S., Janka, H.-T., & Hillebrandt, W. 2006, A&A, 450, 345
Loll, A. M., Desch, S. J., Scowen, P. A., & Foy, J. P. 2013, ApJ, 765, 152
Lundqvist, P., Fransson, C., & Chevalier, R. A. 1986, A&A, 162, L6
Lundqvist, P., & Tziambazis, A. 2012, MNRAS, 423, 1571
Lyne, A. G., Pritchard, R. S., & Smith, F. G. 1988, MNRAS, 233, 667
Matzner, C. D., & McKee, C. F. 1999, ApJ, 510, 379
Mauerhan, J. C., Smith, N., Silverman, J. M., et al. 2013, MNRAS, 431, 2599
Moriya, T. J., Tominaga, N., Langer, N., et al. 2014, A&A, 569, AA57
Nomoto, K., Sugimoto, D., Sparks, W. M., et al. 1982, Natur, 299, 803
Nugent, R. L., 1998, PASP, 110, 831
Owen, P. J., & Barlow, M. J. 2015, ApJ, 801, 141
Radie, G. C., Fesen, R. A., & Yamada, T. 2008, MNRAS, 384, 1200
Sankrit, R., & Hester, J. J. 1997, ApJ, 491, 796
Seward, F. D., Gorenstein, P., & Smith, R. K. 2006, ApJ, 636, 873
Smith, N. 2013, MNRAS, 434, 102
Sollerman, J., Lundqvist, P., Lindler, D., et al. 2000, ApJ, 537, 861
Temim, T., Gehrz, R. D., Woodward, C. E., et al. 2006, AJ, 132, 1610
Tominaga, N., Blinnikov, S. I., & Nomoto, K. 2013, ApJL, 771, L12
Trimble, V. 1968, AJ, 73, 535
Trimble, V. 1973, PASP, 85, 579
Wang, X., Ferland, G. J., Baldwin, J. A., Loh, E. D., & Richardson, C. T. 2013, ApJ, 774, 112
Wyckoff, S., & Murray, C. A. 1977, MNRAS, 180, 717