Computing Banhatti Indices of Hexagonal, Honeycomb and Derived Networks

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Abstract: Banhatti indices of a graph were introduced by Kulli. In this paper we have computed the general K-Banhatti indices, first and second K-Banhatti indices, K hyper Banhatti indices, modified K Banhatti indices and sum connectivity Banhatti indices for hexagonal, honeycomb and honeycomb derived networks.

Keywords: Banhatti Indices, K-Banhatti Indices, K-Hyper Banhatti Indices, Modified K Banhatti Indices, Hexagonal and Honeycomb Networks

1. Introduction

Kulli introduced the first and second K-Banhatti indices of a graph in [1]. These are defined as,

$$B_1(G) = \sum_{u \in V(G)} d(u) + d(e) \quad \text{and} \quad B_2(G) = \sum_{u \in V(G)} d(u) d(e)$$

where $u e$ indicate that the vertex $u$ and edge $e$ are incident in $G$. Kulli also defined some properties of these newly defined indices. The coindices of K-Banhatti indices were also defined in his work. Later Kulli defined K hyper-Banhatti indices of V-Phenylenic nanotubes and nanotorus [2]. Gutman et al developed relations between Banhatti and Zagreb indices and discussed the lower and upper bounds for Banhatti indices of a connected graph in terms of Zagreb indices [3]. Kulli et al also computed Banhatti indices for certain families of benzenoid systems [4]. Moreover, Kulli introduced multiplicative hyper-Banhatti indices and coindices, Banhatti geometric-arithmetic index connectivity Banhatti indices for certain families of benzenoid systems [5-7]. The Banhatti indices were also introduced and computed by Kulli [8].

Graph theory has found considerable use in modeling chemical structures. Chemical graph theory is an important branch of mathematical chemistry that uses graph theory in the mathematical modeling of chemical phenomena. Chemical graph theory has an important effect in the development of mathematical chemistry and chemical sciences.

Computing topological indices in mathematical chemistry is an important branch. Topological index has become a very useful tool in the prediction of physio chemical and pharmacological properties of a compound.

The number of vertices and edges are the topological index molecular structure matters. The main ingredients of the molecular topological models are topological indices which are the topological characterization of molecules by means of numerical invariants. These models are instrumental in the discovery of new applications of molecules with specific chemical, pharmacological and biological properties. Applications of graph theory have led to the emergence of a number of graph-theoretical indices [9]. These indices are used by various researchers in their studies. The first use of a topological index was made by the chemist Harold Wiener in 1947 [10]. In recent years many researchers have worked on computing topological indices [11-19]. Bharati, R. et al. have calculated the Zagreb, Randić, and ABC index of silicate, honeycomb and hexagonal networks [20].
molecular graph and calculated atom bond connectivity reverse index and product connectivity reverse index for oxide and honeycomb networks [21], the direct and inverse sum Banhatti indices for some graphs [22], multiplicative connectivity banhatti indices of benzenoid systems and polycyclic aromatic hydrocarbons [23] and reverse zagreb and reverse hyper-zagreb indices and their polynomials of rhombus silicate networks [24].

S. Hayat et al. [25] derived some new classes of networks from honeycomb network by using some basic graph operations like stellation, bounded dual and medial of a graph and denoted these n-dimensional honeycomb derived network of first type as $HcDN1(n)$. We give analytic formulas of the general K-Banhatti indices, first and second K-Banhatti indices, K hyper Banhatti indices, modified K Banhatti indices and sum connectivity Banhatti indices of the hexagonal, honeycomb and derived networks.

2. Calculating Banhatti Indices for the Hexagonal Network

Triangular, square, and hexagonal are three regular plane tessellations, composed of the same kind of regular polygons. The triangular tessellation is used to define Hexagonal network and this is widely studied in [26]. A hexagonal network is shown in figure 1. There are three types of vertices based on their degree in a hexagonal network. There are only 6 vertices of degree 3, 612 vertices of degree 4 and 3n² − 9n + 7 vertices of degree 6.

The general first and second K-Banhatti indices of a graph are defined as:

$$B_1^a(G) = \sum_{ue}[d_G(u) + d_G(e)]^a$$  \hspace{3cm} (1)

$$B_2^a(G) = \sum_{ue}[d_G(u)d_G(e)]^a,$$  \hspace{3cm} (2)

$$B_1^aHX(n) = 12(8^a + 9^a) + 6(10^a + 13^a) + 12(n - 3)10^a + 12(n - 2)(12^a + 14^a) + 2(9n^2 - 33n + 30)16^a$$  \hspace{3cm} (3)

$$SB_2^aHX(n) = 12(15^a + 20^a) + 6(21^a + 42^a) + 12(n - 3)24^a + 12(n - 2)(32^a + 48^a) + 2(9n^2 - 33n + 30)60^a$$  \hspace{3cm} (4)

Proof: Let $G$ be the graph of hexagonal network $HX(n)$ of dimension $n$, with $|V(HX(n))| = 3n^2 - 3n + 1$ and $|E(HX(n))| = 9n^2 - 15n + 6$, where $n$ is the number of vertices on one side of the hexagon. There are five type of edges based on degree of end vertices in a hexagonal network shown in table 1.

(a) We compute $B_1^aHC(n)$ as follows:

$$B_1^a(HX(n)) = \sum_{ue}[d_G(u) + d_G(e)]^a$$

$$= 12(8^a + 9^a) + 6(10^a + 13^a) + 12(n - 3)10^a + 12(n - 2)(12^a + 14^a) + (9n^2 - 33n + 30)16^a$$

(b) We compute $B_2^aHC(n)$ as follows:

$$B_2^a(HX(n)) = \sum_{ue}[d_G(u)d_G(e)]^a$$

$$= 12(15^a + 20^a) + 6(21^a + 42^a) + 12(n - 3)24^a + 12(n - 2)(32^a + 48^a) + 2(9n^2 - 33n + 30)60^a$$

Corollary: The first and second K-Banhatti indices for a hexagonal network $HX(n)$ are given by

$$B_1(HX(n)) = 4608n^2 - 16464n + 14718$$  \hspace{3cm} (5)
Proof: Putting $a = 1$ in equation (3), we get

$$B_4(HX(n)) = 64800n^2 - 236352n + 214014$$  \hspace{1cm} (6)$$

Putting $a = 1$ in equation (4), we get

$$= 12(17) + 6(23) + 120(n - 3) + 312(n - 2) + 512(9n^2 - 33n + 30) = 4608n^2 - 16464n + 14718$$

Corollary: The first and second K-hyper Banhatti indices for a hexagonal network $HX(n)$ are given by

$$HB_1(HX(n)) = 4608n^2 - 11616n + 6954$$  \hspace{1cm} (7)$$

$$HB_2(HX(n)) = 64800n^2 - 190752n + 136122$$  \hspace{1cm} (8)$$

Proof: Putting $a = 2$ in equation (3), we get

$$= 1740 + 1614 + 1200n - 3600 + 4080(n - 2) + 4608n^2 - 16896n + 15360 = 4608n^2 - 11616n + 6954$$

Putting $a = 2$ in equation (4), we get

$$= 7500 + 13230 + 6912 - 20736 + 39936 - 79872 + 64800n^2 - 237600 + 216000 = 64800n^2 - 190752n + 136122$$

Corollary: The first and second modified K Banhatti indices for a hexagonal network $HX(n)$ are given by

$$mB_1(HX(n)) = \frac{9}{8}n^2 - \frac{299}{8}n + \frac{361}{1092}$$  \hspace{1cm} (9)$$

$$mB_2(HX(n)) = \frac{3}{10}n^2 + \frac{1}{40}n + 140$$  \hspace{1cm} (10)$$

Proof: Putting $a = -1$ in equation (3), we get

$$= 12\left(\frac{1}{8} + \frac{1}{9}\right) + 6\left(\frac{1}{10} + \frac{1}{13}\right) + 12\left(\frac{n - 3}{10}\right) + 12\left(n - 2\right)\left(\frac{1}{12} + \frac{1}{14}\right) + \frac{1}{8}(9n^2 - 33n + 30) = \frac{9}{8}n^2 - \frac{299}{8}n + \frac{361}{1092}$$

Putting $a = -1$ in equation (4), we get

$$= 12\left(\frac{1}{15} + \frac{1}{20}\right) + 6\left(\frac{1}{21} + \frac{1}{42}\right) + \frac{1}{2}(n - 3) + 12\left(n - 2\right)\left(\frac{1}{32} + \frac{1}{48}\right) + \frac{1}{30}(9n^2 - 33n + 30) = \frac{3}{10}n^2 + \frac{1}{40}n + 140$$

Corollary: The first and second sum connectivity Banhatti indices for a hexagonal network $HX(n)$ are given by

$$SB_1(HX(n)) = 4.5n^2 - 6.03403029n - 9.106540386$$  \hspace{1cm} (11)$$

$$SB_2(HX(n)) = 2.323790008n^2 - 2.217702468n - 2.390835824$$  \hspace{1cm} (12)$$

Proof: Putting $a = -\frac{1}{2}$ in equation (3), we get

$$= 12\left(\frac{1}{\sqrt{8}} + \frac{1}{\sqrt{9}}\right) + 6\left(\frac{1}{\sqrt{10}} + \frac{1}{\sqrt{13}}\right) + 12\left(\frac{n - 3}{\sqrt{10}}\right) + 12\left(n - 2\right)\left(\frac{1}{\sqrt{12}} + \frac{1}{\sqrt{14}}\right) + \frac{1}{2}(9n^2 - 33n + 30)$$

Putting $a = -\frac{1}{2}$ in equation (4), we get

$$= 12\left(\frac{1}{\sqrt{15}} + \frac{1}{\sqrt{20}}\right) + 6\left(\frac{1}{\sqrt{21}} + \frac{1}{\sqrt{42}}\right) + 12\left(n - 3\right) + 12\left(n - 2\right)\left(\frac{1}{\sqrt{23}} + \frac{1}{\sqrt{48}}\right) + \frac{2}{\sqrt{60}}(9n^2 - 33n + 30)$$

$$= \frac{9}{2}n^2 + \left(\frac{12}{\sqrt{10}} + \frac{12}{\sqrt{12}} + \frac{12}{\sqrt{14}} + \frac{33}{2}\right)n + 4 + 6\left(\frac{12}{\sqrt{10}} + \frac{12}{\sqrt{13}} + \frac{12}{\sqrt{14}} - \frac{36}{\sqrt{12}} - \frac{42}{\sqrt{14}} + 15\right)$$

Putting $a = -\frac{1}{2}$ in equation (4), we get

$$= \frac{18}{\sqrt{60}}n^2 + \left(\frac{12}{\sqrt{24}} + \frac{12}{\sqrt{32}} + \frac{12}{\sqrt{48}} + \frac{66}{\sqrt{60}}\right)n + \frac{12}{\sqrt{20}} + \frac{6}{\sqrt{21}} + \frac{6}{\sqrt{24}} - \frac{36}{\sqrt{24}} - \frac{24}{\sqrt{32}} - \frac{24}{\sqrt{48}} + \frac{60}{\sqrt{60}}$$

$$= 4.5n^2 - 6.03403029n - 9.106540386$$
3. Calculating Banhatti Indices for the Honeycomb Network

A honeycomb network $HC(n)$ is obtained from $HC(n-1)$ by adding a layer of hexagons around the boundary of $HC(n-1)$, where $n$ determines the number of hexagons between the boundary and center of $HC(n)$. Honeycomb networks are used in image processing, mobile phone base stations and computer graphics. In chemistry it is used as a representation of benzenoid hydrocarbons.

A honeycomb network is shown in figure 2. There are $6n$ vertices of degree 2 and the remaining vertices are of degree 3.

| $d_4(u), d_4(e)$ | $d_6(e)$ | $|E(RHOX(n))|$ |
|------------------|----------|----------------|
| (2,2)            | 2        | 6              |
| (2,3)            | 3        | $12(n-1)$      |
| (3,3)            | 4        | $(9n^2 - 15n + 6)$ |

Theorem: For a honeycomb network $HC(n)$ of dimension $n$, the general first and second K-Banhatti indices are given by

$$B_1^aHC(n) = 12 \times 4^a + 12(n-1)(5^a + 6^a) + 2(9n^2 - 15n + 6)7^a$$

$$B_2^aHC(n) = 12 \times 4^a + 12(n-1)(6^a + 9^a) + 2(9n^2 - 15n + 6)12^a$$

(13) (14)

Proof: Let $G$ be the graph of honeycomb network $HC(n)$ of dimension $n$, with $|V(HC(n))| = 6n^2$ and $|E(HC(n))| = 9n^2 - 3n$. There are three types of edges based on degree of end vertices in a honeycomb network shown in table 2.

a) We compute $B_1^aHC(n)$ as follows:

$$B_1^a(HC(n)) = \sum u \in G \sum e \in G d_4(u) + d_6(e)$$

$$= 6(4^a + 4^a) + 12(n-1)(5^a + 6^a) + (9n^2 - 15n + 6)(7^a + 7^a)$$

$$= 12 \times 4^a + 12(n-1)(5^a + 6^a) + 2(9n^2 - 15n + 6)7^a$$

b) We compute $B_2^aHC(n)$ as follows:

$$B_2^a(HX(n)) = \sum u \in G \sum e \in G d_4(u)d_6(e)$$

$$= 12(4^a+4^a) + 12(n-1)(6^a + 9^a) + (9n^2 - 15n + 6)(12^a + 12^a)$$

$$= 12 \times 4^a + 12(n-1)(6^a + 9^a) + 2(9n^2 - 15n + 6)12^a$$

Corollary: The first and second K-Banhatti indices for a honeycomb network $HC(n)$ are given by

$$B_1(HC(n)) = 129n^2 - 78n$$

$$B_2(HC(n)) = 216n^2 - 180n + 12$$

(15) (16)

Proof: Putting $a = 1$ in equation (13), we get

$$= 48 + 132(n-1) + 14(9n^2 - 15n + 6) = 129n^2 - 78n$$

Putting $a = 1$ in equation (14), we get

$$= 48 + 180(n-1) + 24(9n^2 - 15n + 6) = 216n^2 - 180n + 12$$

Corollary: The first and second K-hyper Banhatti indices for a honeycomb network $HC(n)$ are given by

$$HB_1(HC(n)) = 882n^2 - 738n + 48$$

$$HB_2(HC(n)) = 2592n^2 - 2916n + 516$$

(17) (18)

Proof: Putting $a = 2$ in equation (13), we get
Putting \( a = 2 \) in equation (14), we get
\[
= 192 + 732(n - 1) + 98(9n^2 - 15n + 6) = 882n^2 - 738n + 48
\]

Putting \( a = 2 \) in equation (14), we get
\[
= 192 + 1404(n - 1) + 288(9n^2 - 15n + 6) = 2592n^2 - 2916n + 516
\]

Corollary: The first and second modified K Banhatti indices for a honeycomb network \( HC(n) \) are given by
\[
mB_1(HC(n)) = \frac{18}{7} n^2 + \frac{4}{35} n + \frac{11}{35}
\]
\[
mB_2(HC(n)) = \frac{3}{2} n^2 + \frac{5}{6} n + \frac{2}{3}
\]

Proof: Putting \( a = -1 \) in equation (13), we get
\[
= 3 + 12(n - 1)\left(\frac{1}{5} + \frac{1}{6}\right) + 2\left(9n^2 - 15n + 6\right) = \frac{18}{7} n^2 + \frac{4}{35} n + \frac{11}{35}
\]

Putting \( a = -1 \) in equation (14), we get
\[
= 3 + 12(n - 1)\left(\frac{1}{6} + \frac{1}{9}\right) + \frac{1}{6} (9n^2 - 15n + 6) = \frac{3}{2} n^2 + \frac{5}{6} n + \frac{2}{3}
\]

Corollary: The first and second sum connectivity Banhatti indices for a honeycomb network \( HC(n) \) are given by
\[
SB_1(HC(n)) = 6.803360514n^2 - 1.073391559n + 15.43455316
\]
\[
SB_2(HC(n)) = 5.196152423n^2 + 0.2387254477n + 0.5651221296
\]

Proof: Putting \( a = -\frac{1}{2} \) in equation (13), we get
\[
= \frac{12}{\sqrt{4} + 12(n - 1)\left(\frac{1}{\sqrt{5}} + \frac{1}{\sqrt{6}}\right) + \frac{2}{\sqrt{7}} (9n^2 - 15n + 6)}
\]
\[
= \frac{12}{\sqrt{7} n^2 + \left(2\sqrt{5} + \frac{12\sqrt{5}}{5} - \frac{30}{\sqrt{7}}\right) n + 6 + 2\sqrt{6} + \frac{12}{\sqrt{7}}}
\]
\[
= 6.803360514n^2 - 1.073391559n + 15.43455316
\]

Putting \( a = -\frac{1}{2} \) in equation (14), we get
\[
= \frac{12}{\sqrt{4} + 12(n - 1)\left(\frac{1}{\sqrt{6}} + \frac{1}{\sqrt{9}}\right) + \frac{2}{\sqrt{12}} (9n^2 - 15n + 6)}
\]
\[
= \frac{12}{\sqrt{12} n^2 + \left(\frac{12}{\sqrt{6}} + 4 - \frac{30}{\sqrt{12}}\right) n + 2 - \frac{12}{\sqrt{6}} + \frac{12}{\sqrt{12}}}
\]
\[
= 5.196152423n^2 + 0.2387254477n + 0.5651221296
\]

4. Calculating Banhatti Indices for the Honeycomb Derived Networks

In figure 3 a honeycomb derived network \( HcDN1(n) \) with dimension 3 is given, where the black colored graph is 3-dimensional honeycomb network and blue colored graph is its stellation. Now we compute the general K-Banhatti indices, first and second K-Banhatti indices, K hyper Banhatti indices, modified K Banhatti indices and sum connectivity Banhatti indices of the honeycomb derived networks. First, we compute these indices for honeycomb derived network of first type, \( HcDN1(\text{I}) \) in the following theorem.

Theorem: For a honeycomb derived network \( HcDN1(n) \), the general first and second K-Banhatti indices are given by

Figure 3. Honeycomb derived network \( HcDN1 \) with dimension 3.
Proof: We compute the required results as follows:

(i) To compute $B_1^a(HcDN1(n))$,

$$B_1^a(HcDN1(n)) = 12 \times 7^a + 12(n - 1)(9^a + 11^a) + 6n(10^a + 13^a) + 18(n - 1)(14^a + 15^a) + 2(27n^2 - 57n + 130) \times 16^a \quad (23)$$

(ii) To compute $B_2^a(HcDN1(n))$,

$$B_2^a(HcDN1(n)) = 12 \times 12^a + 12(n - 1)(18^a + 30^a) + 6n(21^a + 42^a) + 18(n - 1)(45^a + 54^a) + 2(27n^2 - 57n + 130) \times 60^a \quad (24)$$

Corollary: The first and second K-Banhatti indices for a honeycomb derived network $HcDN1(n)$ are given by

$$B_1(HcDN1(n)) = 864n^2 - 924n + 282 \quad (25)$$

$$B_2(HcDN1(n)) = 3240n^2 - 4104n + 1386 \quad (26)$$

Proof: Putting $a = 1$ in equation (23), we get

$$= 12 \times 7 + 12(n - 1)(9 + 11) + 6n(10 + 13) + 18(n - 1)(14 + 15) + 2(27n^2 - 57n + 130) \times 16$$

Putting $a = 1$ in equation (24), we get

$$= 12 \times 12 + 12(n - 1)(18 + 30) + 6n(21 + 42) + 18(n - 1)(45 + 54) + 2(27n^2 - 57n + 130) \times 60$$

Corollary: The first and second K-hyper Banhatti indices for a honeycomb derived network $HcDN1(n)$ are given by

$$HB_1(HcDN1(n)) = 1382n^2 - 17586n + 5946 \quad (27)$$

$$HB_2(HcDN1(n)) = 194400n^2 - 293544n + 114102 \quad (28)$$

Proof: Putting $a = 2$ in equation (23), we get

$$= 12 \times 49 + 12(n - 1)(81 + 121) + 6n(100 + 169) + 18(n - 1)(196 + 225) + 2(27n^2 - 57n + 130) \times 256$$

Putting $a = 2$ in equation (24), we get

$$= 12 \times 144 + 12(n - 1)(18^2 + 30^2) + 6n(21^2 + 42^2) + 18(n - 1)(45^2 + 54^2) + 2(27n^2 - 57n + 130) \times 60^2$$

Corollary: The first and second modified K Banhatti indices for a honeycomb derived network $HcDN1(n)$ are given by

$$mB_1(HcDN1(n)) = 3.375n^2 - 1.153504829n + 13.054329 \quad (29)$$

$$mB_2(HcDN1(n)) = \frac{9}{10}n^2 + \frac{23}{70}n + \frac{1}{5} \quad (30)$$

Proof: Putting $a = -1$ in equation (23), we get

$$= \frac{12}{7} + 12(n - 1)\left(\frac{1}{9} + \frac{1}{11}\right) + 6n\left(\frac{1}{10} + \frac{1}{13}\right) + 18(n - 1)\left(\frac{1}{14} + \frac{1}{15}\right) + \frac{2}{16}(27n^2 - 57n + 130)$$

Putting $a = -1$ in equation (24), we get
\[
= \frac{12}{12} + 12(n-1)\left(\frac{1}{18} + \frac{1}{30}\right) + 6n\left(\frac{1}{21} + \frac{1}{42}\right) + 18(n-1)\left(\frac{1}{45} + \frac{1}{54}\right) + \frac{2}{60}(27n^2 - 57n + 130)
\]

\[
= \frac{9}{10}n^2 + \frac{23}{70}n + \frac{1}{5}
\]

Corollary: The first and second sum connectivity Banhatti indices for a honeycomb derived network \(HcDN1(n)\) are given by

\[
SB_1(HcDN1(n)) = 13.5n^2 - 1.86211431n + 52.45915517
\]

\[
SB_2(HcDN1(n)) = 6.971370023n^2 - 2.33012604n + 26.87786861
\]

Proof: Putting \(a = -\frac{1}{2}\) in equation (23), we get

\[
\frac{12}{\sqrt{7}} + 12(n-1)\left(\frac{1}{\sqrt{9}} + \frac{1}{\sqrt{11}}\right) + 6n\left(\frac{1}{\sqrt{10}} + \frac{1}{\sqrt{13}}\right) + 18(n-1)\left(\frac{1}{\sqrt{14}} + \frac{1}{\sqrt{15}}\right) + \frac{2}{\sqrt{16}}(27n^2 - 57n + 130)
\]

\[
= 13.5n^2 - 1.86211431n + 52.45915517
\]

Putting \(a = -\frac{1}{2}\) in equation (24), we get

\[
\frac{12}{\sqrt{12}} + 12(n-1)\left(\frac{1}{\sqrt{16}} + \frac{1}{\sqrt{30}}\right) + 6n\left(\frac{1}{\sqrt{21}} + \frac{1}{\sqrt{42}}\right) + 18(n-1)\left(\frac{1}{\sqrt{45}} + \frac{1}{\sqrt{54}}\right) + \frac{2}{\sqrt{60}}(27n^2 - 57n + 130)
\]

\[
= 6.971370023n^2 - 2.33012604n + 26.87786861
\]

5. Conclusion

In this paper hexagonal, honeycomb and honeycomb derived network \(HcDN1(n)\) are studied and the analytical closed formulas are determined for the general K-Banhatti indices, first and second K-Banhatti indices, K hyper Banhatti indices, modified K Banhatti indices and sum connectivity Banhatti indices of hexagonal, honeycomb and honeycomb derived network \(HcDN1(n)\). It will help to understand the physical features, chemical reactivities and biological activities of the hexagonal and honeycomb and honeycomb derived network \(HcDN1(n)\). These results can provide a significant determination in the pharmaceutical industry.

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