ON REMOVING INTERLOPER CONTAMINATION FROM INTENSITY MAPPING
POWER SPECTRUM MEASUREMENTS

ADAM LIDZ AND JESSIE TAYLOR
Department of Physics & Astronomy, University of Pennsylvania, 209 South 33rd Street, Philadelphia, PA 19104, USA; alidz@sas.upenn.edu
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ABSTRACT
Line intensity mapping experiments seek to trace large-scale structures by measuring the spatial fluctuations in the combined emission, in some convenient spectral line, from individually unresolved galaxies. An important systematic concern for these surveys is line confusion from foreground or background galaxies emitting in other lines that happen to lie at the same observed frequency as the “target” emission line of interest. We develop an approach to separate this “interloper” emission at the power spectrum level. If one adopts the redshift of the target emission line in mapping from observed frequency and angle on the sky to co-moving units, the interloper emission is mapped to the wrong co-moving coordinates. Because the mapping is different in the line of sight and transverse directions, the interloper contribution to the power spectrum becomes anisotropic, especially if the interloper and target emission are at widely separated redshifts. This distortion is analogous to the Alcock–Paczynski test, but here the warping arises from assuming the wrong redshift rather than an incorrect cosmological model. We apply this to the case of a hypothetical [C II] emission survey at $z \sim 7$ and find that the distinctive interloper anisotropy can, in principle, be used to separate strong foreground CO emission fluctuations. In our models, however, a significantly more sensitive instrument than currently planned is required, although there are large uncertainties in forecasting the high-redshift [C II] emission signal. With upcoming surveys, it may nevertheless be useful to apply this approach after first masking pixels suspected of containing strong interloper contamination.

Key words: cosmology: theory – dark ages, reionization, first stars – intergalactic medium – large-scale structure of universe

1. INTRODUCTION
Intensity Mapping (IM) is an appealing approach for studying the large-scale structure of the universe and for characterizing the bulk properties of galaxy populations emitting in various spectral lines across cosmic time. IM observations forego detecting galaxies individually. Instead, one measures the large-scale spatial fluctuations in the collective emission from all of the luminous sources emitting in some convenient spectral line or lines (see e.g., Sugino et al. 1999; Chang et al. 2008; Righi et al. 2008; Visbal & Loeb 2010; Carilli 2011; Gong et al. 2011; Lidz et al. 2011; Pullen et al. 2013; Breyesse et al. 2014; Uzgil et al. 2014; Croft et al. 2015; Keating et al. 2015; Mashian et al. 2015; Li et al. 2016). This complements traditional galaxy surveys which target individual objects in that IM surveys are sensitive to the collective emission from all luminous sources, while traditional observations are limited to detecting only those sources that lie above survey flux limits. IM also probes line emission across a range of large-scale environments, and is sensitive to the emission from galaxies in underdense voids as well as sources in high-density peaks. This is often impossible in a traditional survey, where spanning large-scale environmental variations requires capturing an enormous volume at high sensitivity.

One potentially powerful application is to the Epoch of Reionization (EoR). Current evidence suggests that the universe is reionized largely by numerous low-luminosity sources (e.g., Robertson et al. 2015), so it is extremely challenging to detect most of the ionizing sources individually. However, it may nevertheless be possible to study their collective impact using IM. In addition, by spanning a large field of view at coarse angular resolution while retaining redshift information, IM surveys would be well-matched to redshifted 21 cm observations of the EoR. The cross-correlation of IM measurements with redshifted 21 cm data sets could then be used to confirm the high-redshift origin of a putative 21 cm signal from the EoR (Furlanetto & Lidz 2007; Lidz et al. 2009, 2011). Only the high-redshift portion of the redshifted 21 cm signal, and not residual foreground emission, should correlate with the IM data (asides for shared foregrounds). Furthermore, the scale-dependence of the cross-correlation between the two signals provides a powerful probe of the size of the ionized regions that form around groups of galaxies during reionization (Lidz et al. 2009, 2011; Gong et al. 2011).

One systematic concern with IM measurements relates to foreground interloper emission (Visbal & Loeb 2010). This interloper emission arises from sources residing at lower (or possibly higher) redshifts—and emitting in different lines—than targeted by the IM survey, with the interlopers nevertheless contributing to the specific intensity at the observed wavelengths of interest. Explicitly, suppose the survey targets an emission line with a rest-frame wavelength of $\lambda_{r,i}$ and a target redshift around $z_t$. The observed wavelength of this emission is $\lambda_{\text{obs}} = \lambda_{r,i}(1 + z_t)$. Clearly, an interloper source emitting in a line with rest wavelength $\lambda_{r,a}$ can emit at the same observed wavelength provided its redshift, $z_a$, satisfies $1 + z_a = \lambda_{r,a}(1 + z_t)/\lambda_{r,i}$. One approach to avoid bias from interloper emission is to probe two different emission lines from gas at the same redshift. The cross-correlation between the emission at the two corresponding observed wavelengths will, on average, only pick up contributions from gas at the target redshift (e.g., Visbal & Loeb 2010). Although each of the two observed wavelengths will contain interloper emission, the
interlopers will be at widely separated redshifts and so uncorrelated. It will likely, however, be valuable to have additional handles to discriminate interloper emission. For one, it may not be feasible for the IM surveys to capture multiple bright lines from the same emitting gas, since this requires high sensitivity over a broad range of wavelengths. Moreover, it is necessary to clean interloper contamination to measure the auto spectrum of the emission fluctuations in a line of interest; this quantity contains information that is not available from the cross spectrum between two lines. Explicitly, as we will describe (see Equations (10) and (27)), the large-scale cross spectrum between two lines depends (mostly) on the product of the specific intensity and luminosity-weighted bias factor in each line while the auto spectrum depends on the product of the specific intensity and luminosity-weighted bias in the single emission line of interest. On small scales, the shot-noise term in the cross spectrum depends on the degree of overlap between the galaxy populations emitting in each line, while the shot-noise contribution to the auto spectrum is determined solely by the second moment of the luminosity function in the line. Put more generally, the auto spectrum depends only on the emission in a single line while the cross spectrum depends on the emission properties in two lines and therefore has a less direct interpretation.

Another possible approach is to mask out regions suspected of containing bright interloper emission, but this may require an additional survey to identify which regions to mask (e.g., Silva et al. 2015). The second survey must span the redshift range of all prominent interloper lines, and trace some quantity that is a good proxy for the interloper line emission. Furthermore, redshift information is required for all of the tracer galaxies. For some applications, it may be necessary to mask a significant fraction of the observed pixels. Finally, the resulting mask will reflect the clustering of the interloper sources; it must be deconvolved carefully to avoid introducing any bias in the inferred target emission fluctuations.

Here, we develop an alternative approach for separating out interloper contamination at the power spectrum level. Our starting point is to note that the mappings between observed wavelength/frequency and angle on the sky to co-moving length scales/wavenumbers are redshift dependent. If we assume the target redshift in converting between the observed frequencies and angles and co-moving coordinates, the interloper fluctuations will be mapped to the wrong wavenumbers. Since the remapping is different for the line of sight and transverse wavenumbers, the interloper contribution to the observed power spectrum will have a distinctive anisotropy. This is analogous to the Alcock–Paczynski (AP) effect (Alcock & Paczynski 1979; Ballinger et al. 1996), except in the case of the AP test a warping arises from assuming the wrong cosmology, while here the distortion results from adopting the incorrect redshift. We will show that this transfer of power and warping can be used to separate out the interloper contamination. This basic idea is mentioned in previous work by Visbal & Loeb (2010) and Gong et al. (2014), but we develop the technique further here and apply it to quantify the prospects for cleaning interloper lines from future $z \sim 7$ [C II] surveys. Although we focus on the illustrative example of IM with the [C II] line, our approach should be broadly applicable to IM surveys in other lines such as Lyα and CO transitions, and may also be of interest for traditional surveys detecting line-emitting galaxies.

The outline of this paper is as follows. In Section 2 we describe and quantify the interloper distortion. This is then applied to the example case of a futuristic $z \sim 7$ [C II] emission survey (Section 3). Section 4 forecasts the constraints on [C II] and CO emission line properties that may be achieved by this survey. We further consider combining our technique with additional tracers of large-scale structure at the redshifts of prominent foreground interlopers (Section 5). We also discuss the prospects for cross-correlating with other emission lines at $z \sim 7$ (Section 6). We conclude in Section 7. Throughout we adopt a cosmological model with $\Omega_m = 0.27$, $\Omega_m = 0.073$, $\Omega_b = 0.046$, $h = 0.7$, $\sigma_8(z = 0) = 0.8$, and $n_s = 1$, broadly consistent with recent Planck measurements (Ade et al. 2013).

2. INTERLOPER COORDINATE MAPPING DISTORTIONS

In order to illustrate the technique, let us first suppose that our data cube contains only two sources of line emission: our target line of interest at redshift $z_t$ and a single dominant interloper line at redshift $z_i$. We will soon generalize to the case that several interloper lines contribute. We denote the observed frequency at the center of the data cube by $\nu_{\text{obs}}$ and consider emission offset by a small frequency interval $\Delta \nu_{\text{obs}}$ from the cube center. Further, let $\Delta \theta$ be the angular separation from the center of the cube; the vector describes the two directions transverse to the line of sight and we work in the flat sky approximation. In order to convert from the observed $\Delta \nu_{\text{obs}}$ and $\Delta \theta$ to co-moving coordinates, we need to assume a cosmological model and a redshift for the emission.

Adopting the target redshift for this mapping will cause the interloper emission to be mapped to the wrong co-moving coordinates. Let us denote the apparent line of sight coordinate for the interloper emission by $\tilde{x}_\parallel$ and the apparent transverse coordinate by $\tilde{x}_\perp$. Further suppose that the true line of sight and transverse coordinates at the interloper redshift are $x_\parallel$ and $x_\perp$. The apparent coordinates are related to the observable frequency interval and angles by incorrectly assuming the emission is at the target redshift:

$$\tilde{x}_\parallel = \frac{c}{H(z_t)} (1 + z_t) \frac{\Delta \nu_{\text{obs}}}{\nu_{\text{obs}}},$$

and

$$\tilde{x}_\perp = D_{A,\text{co}}(z_t) \Delta \theta,$$

where $H(z_t)$ is the Hubble parameter at the target redshift and $D_{A,\text{co}}(z_t)$ is the co-moving angular diameter distance to the target redshift. (For a flat universe, $D_{A,\text{co}}(z_t) = \chi(z_t)$ with $\chi(z_t)$ being the co-moving distance to redshift $z_t$.) The relations between the apparent coordinates, $\tilde{x}_\parallel$ and $\tilde{x}_\perp$, and the true coordinates, $x_\parallel$ and $x_\perp$, are then

$$\tilde{x}_\parallel = \frac{H(z_t)}{H(z_i)} \frac{1 + z_t}{1 + z_i} x_\parallel,$$

and

$$\tilde{x}_\perp = \frac{D_{A,\text{co}}(z_i)}{D_{A,\text{co}}(z_t)} x_\perp.$$

Because we are ultimately interested in the power spectrum, we also consider the line of sight and transverse components of the co-moving wavenumbers. The relevant factors here are just the
inverse of the coordinate mappings

\[ \tilde{k} = \frac{H(z_i)}{H(z_f)} \left( 1 + \frac{z_i}{1 + z_f} \right) k_{\parallel, i} = \alpha_{\parallel} k_{\parallel, i} \]  

and

\[ \tilde{k}_L = \frac{D_{\Delta, co}(z_i)}{D_{\Delta, co}(z_f)} k_L = \alpha_L k_L. \]  

Here, we have defined “distortion” factors, \( \alpha_{\parallel} \) and \( \alpha_L \). These describe the remapping that occurs when the incorrect redshift is used to convert angles and observed frequencies to wavenumbers for the interloper population.

Turning now to power spectrum, we consider the fluctuations in the specific intensity field, \( I_{\text{tot}}(x) \). Note that throughout we will work with this quantity rather than with the power spectrum of \( \beta(x) = (I_{\text{tot}}(x) - \langle I_{\text{tot}} \rangle)/\langle I_{\text{tot}} \rangle \) — i.e., we do not divide out by \( \langle I_{\text{tot}} \rangle \). The apparent power spectrum of the interloper emission is then

\[ P_I(\tilde{k}_{\parallel}, \tilde{k}_L) = \frac{1}{\alpha_{\parallel}^2 \alpha_L^2} P_I \left( \frac{\tilde{k}_{\parallel}}{\alpha_{\parallel}}, \frac{\tilde{k}_L}{\alpha_L} \right). \]  

Here, \( P_I \) is the apparent interloper power spectrum, while \( P_I \) is the true interloper power spectrum. This equation reflects how the power spectrum transforms under a change of coordinates; the \( 1/(\alpha_{\parallel}^2 \alpha_L^2) \) factor is the ratio of the apparent to actual volume surveyed at the interloper redshift (see Ballinger et al. 1996 for a related discussion in the context of the AP effect, and Visbal & Loeb 2010; Gong et al. 2014; Pullen et al. 2016 for earlier work on interloper contamination). With this transformation law in hand—to make our description more compact—we will generally drop the \( (\tilde{k}_{\parallel}, \tilde{k}_L) \) notation and use \( (k_{\parallel}, k_L) \), nevertheless assuming the target redshift to map between wavelength/angle and co-moving units.

The total power spectrum of fluctuations in the specific intensity is then

\[ P_{\text{tot}}(k_{\parallel}, k_L) = P_I(k_{\parallel}, k_L) + \frac{1}{\alpha_{\parallel}^2 \alpha_L^2} P_I \left( \frac{k_{\parallel}}{\alpha_{\parallel}}, \frac{k_L}{\alpha_L} \right). \]  

The first term on the right hand side is the underlying “target” power spectrum that we seek to determine while the second term arises from the distorted interloper contamination. In the case that the target and interloper line redshifts are quite different—as will often be the case for high-redshift IM observations—the distortion factors \( \alpha_{\parallel} \) and \( \alpha_L \) will differ significantly from unity and from each other. Interestingly, the target line is at higher redshift than the interloper lines, \( \alpha_{\parallel} \) will be larger than unity, while \( \alpha_L \) will be smaller than unity. In other words, the interloper fluctuations that appear at a given \( k_{\parallel}, k_L \) arise from modes that have smaller line of sight wavenumber and larger transverse wavenumber than supposed. Provided \( P_I(k_{\parallel}/\alpha_{\parallel}, k_L/\alpha_L) \) is a decreasing function of \( k_{\parallel} \) and \( k_L \), the distortion then enhances the power for line of sight wavenumbers relative to the transverse modes. As we will see, the shifting of power and the anisotropy induced from these coordinate re-mappings may potentially be used to separate out the target and interloper emission at the power spectrum level.

To provide quantitative information, Figure 1 plots the distortion factors as a function of the interloper redshift for a few example target redshifts. Clearly the distortion factors are quite different from unity and from each other in the case that the target and interloper redshifts are widely separated.

Naturally, in the more general case that \( N \) important interlopers contribute to the power spectrum of fluctuations Equation (8) generalizes to

\[ P_{\text{tot}}(k_{\parallel}, k_L) = P_I(k_{\parallel}, k_L) + \sum_{j=1}^{N} \frac{1}{\alpha_{\parallel}(z_j) \alpha_L^2(z_j)} \times P_I \left( \frac{k_{\parallel}}{\alpha_{\parallel}(z_j)}, \frac{k_L}{\alpha_L(z_j)} \right). \]  

Here, the index \( j \) denotes the \( j \)th of the \( N \) interloper lines, \( z_j \) is the redshift of the \( j \)th interloper emission line, \( P_I \) is the specific intensity power spectrum of this emission, and \( \alpha_{\parallel}(z_j), \alpha_L(z_j) \) are the distortion factors which depend on both the redshift of the interloper \( z_j \) and the target redshift \( z_t \). (We suppress the dependence on the target redshift here to make the notation less cumbersome.) This equation assumes that the interlopers and targets are all widely separated in redshift and therefore independent of each other (otherwise there would be cross-terms), which should be an extremely good approximation in the case considered below.

3. EXAMPLE APPLICATION

Although this technique may have a range of applications, we illustrate it through the interesting example case of a hypothetical survey for [C II] emission at \( z_t = 7 \). Before proceeding further, we very briefly comment on the physics and phenomenology of the [C II] emission line. Recall that the ground state configuration of the five electrons in singly ionized Carbon is \( 1s^22s^22p^1 \), so the ground state has total orbital angular momentum \( L = 1 \) and total spin angular...
momentum $S = 1/2$. The [C\textsc{ii}] line is emitted in transitions from the higher energy fine structure level with total—orbital plus spin—angular momentum $J = 3/2$ to the lower energy state with $J = 1/2$, i.e., it is a $^2P_{3/2} \rightarrow ^2P_{1/2}$ transition. The rest-frame wavelength of the transition is $\lambda_c = 157.7$ \mu m, the excitation temperature of [C\textsc{ii}] is 91 K, and the energy required to ionize C\textsc{i} to C\textsc{ii} is 11.2 eV. Since the ionization potential is less than that of neutral hydrogen (13.6 eV) the [C\textsc{ii}] emission traces—in part—neutral phases of the interstellar medium (ISM), while the low excitation temperature allows emission from warm/cool regions of the ISM. Consequently, [C\textsc{ii}] emission may arise from diverse phases of a galaxy’s ISM including photo-dissociation regions at the boundary between molecular clouds and H\textsc{ii} regions; from the cold neutral medium; and from H\textsc{ii} regions and diffuse ionized gas, provided the local UV radiation field is insufficiently hard to doubly ionize carbon (see e.g., the recent review by Carilli & Walter 2013).

In low-redshift galaxies, the [C\textsc{ii}] line is a strong cooling line with a luminosity that is 0.1%-1% of the total far-infrared luminosity from the galaxy (Stacey et al. 1991). Despite the diverse set of conditions that can give rise to [C\textsc{ii}] emission, the line luminosity is fairly well correlated with the star formation rate, at least at low redshift where there are currently good measurements. This is the case even for low-metallicity dwarf galaxies nearby, although the relation shows larger scatter toward low metallicity (De Looze et al. 2014). Recent observations have started to detect [C\textsc{ii}] emission from Lyman-break selected galaxies and quasar host galaxies at $z \geq 6$, although there are also a handful of upper limits tentatively suggesting that high-redshift galaxies may mostly lie below local [C\textsc{ii}] luminosity star formation rate correlations (e.g., Knudsen et al. 2016 and references therein). Hence, it is unclear how luminous reionization-era galaxies will be in the [C\textsc{ii}] line. Naturally, one of the main goals of IM is to provide a census of the total [C\textsc{ii}] emission; while we have much to learn here, this also makes our forecasts uncertain. In this work, we adopt a simplistic approach and assume that local correlations between [C\textsc{ii}] luminosity and star formation rate apply also at high redshift. Likewise, we adopt local correlations to assess the plausible level of interloper contamination. Future targeted observations of individual galaxies using ALMA will be important for refining estimates of the target and interloper line luminosities. It may also be instructive to construct models of the interstellar media of high-redshift galaxies to try and predict the correlations between line luminosity and star formation rate directly (see e.g., Munoz & Furlanetto 2013).

The central observed wavelength and frequency for our $z_\text{c} = 7$ [C\textsc{ii}] survey are $\lambda_{\text{obs}} = 1.26 \times 10^3$ \mu m, and $\nu_{\text{obs}} = 238$ GHz, respectively. The same observed frequencies will be polluted with emission from CO molecules at lower redshift undergoing rotational transitions. A CO molecule transitioning between rotational states $J$ and $J - 1$ emits a photon of rest-frame frequency $\nu_\text{J} = J \times 115$ GHz. As we will see, several different CO transitions may be significant interlopers for a $z_\text{c} = 7$ [C\textsc{ii}] emission survey. In addition to the CO lines, additional atomic fine structure lines may also provide non-negligible interloper emission but, as we detail below, these are subdominant to the CO interlopers in our models.

### 3.1. Target and Interloper Model Power Spectra

To proceed, let us first discuss the general form of the model intensity power spectra for both the target and interloper emission. Incorporating anisotropies from redshift space distortions, our model for the target power spectrum is (Lidz et al. 2011)

$$P_t(k_j, k_c) = \langle \ell \rangle^2 \langle b_i \rangle^2 (1 + \beta \mu^2)^2 D[\mu k \sigma_p(z_i)] P_t(k_j, z_i) + P_{\text{shot}, j}.$$  \hspace{1cm} (10)

Here, $\mu = k_j / k_c$ is the cosine of the angle between the wavevector $k$ and the line of sight direction, $\langle \ell \rangle$ is the average specific intensity of the target emission, and $\langle b_i \rangle$ is the average luminosity-weighted bias of the emitting galaxies. The factor $(1 + \beta \mu^2)^2$ comes from the Kaiser effect (Kaiser 1987), while $D[\mu k \sigma_p]$ quantifies the small scale reduction of redshift-space power from the finger-of-god effect. The parameter $\beta = f_\text{fz} / f_\text{bt}$ with $f_\text{fz} = \frac{\delta m}{\delta \ln a}$ denoting the usual logarithmic derivative of the growth factor, which is well approximated by $f_\text{fz} \approx \left[ \Omega_m(z)^{0.55} \right]$ (Linder 2005). For the finger-of-god suppression, we assume a Lorentzian form:

$$D[\mu k \sigma_p] = \frac{1}{1 + \sigma_p^2 \mu^2 k^2},$$  \hspace{1cm} (11)

and approximate the pairwise velocity dispersion by $\sigma_p(z) = \sigma_\text{v}(z) / \sqrt{2}$ with $\sigma_\text{v}(z)$ being the variance of the line-of-sight component of the velocity field according to linear theory. In our model, we assume pure linear biasing so that $P_t(k, z_i)$ denotes the matter power spectrum according to linear theory. Finally, $P_{\text{shot}, j}$ is a shot-noise term that arises because the [C\textsc{ii}] emitting galaxies are discrete objects. This term is assumed to be independent of scale. Note that we are taking a somewhat simplified model for the redshift-space emission power spectrum: for the most part, we work on scales much larger than that of individual halos, but we nevertheless include a finger of god term (owing to virialized motions within halos). Although this is a bit inconsistent, the measurements we consider are mostly confined to large scales where the finger-of-god suppression and the halo profile have negligible impact. In future work, it may be interesting to refine this model (see e.g., Cooray & Sheth 2002).

Equation (10) also highlights another potential benefit of measuring the angular dependence of the power spectrum. Although the first term in this equation depends mostly on the product of $\langle \ell \rangle$ and $\langle b_i \rangle$, there is an additional separate dependence on $\langle b_i \rangle$ through the parameter $\beta$. If the angular dependence of the power spectrum can be measured well enough, this should help in breaking the otherwise perfect degeneracy between $\langle \ell \rangle$ and $\langle b_i \rangle$, and allow one to constrain each of these quantities separately (Lidz et al. 2011).

Similarly, the true interloper power spectrum for the $j$th interloper (see Equation (9)) may be written as a function of the true underlying wavenumber components, $k_j$ and $k_c$, as

$$P_j(k_j, k_c) = \langle \ell \rangle^2 \langle b_i \rangle^2 (1 + \beta \mu^2)^2 D[\mu k \sigma_p(z_i)] P_t(k_j, z_i) + P_{\text{shot}, j}.$$  \hspace{1cm} (12)

The apparent interloper power is $1/(c_\text{z}(z)^2) P_j(k_j / c_\text{z}(z), k_c / c_\text{z}(z))$, where we momentarily suppress the $j$ indices on the distortion factors. Note that under the coordinate transformation
of Equations (1)–(6), \( \mu \) maps to \( \mu \rightarrow (k_0/\alpha_0)/\sqrt{(k_1/\alpha_0)^2 + (k_2/\alpha_0)^2} \).

Our model for the total power is then specified by the average specific intensity of the target and interloper emission, \( \langle I_t \rangle \) and \( \langle I_j \rangle \), the luminosity-weighted average bias factors, \( \langle b_t \rangle \) and \( \langle b_j \rangle \), and the shot-noise terms, \( P_{\text{shot,t}} \) and \( P_{\text{shot,j}} \). For simplicity, we generally fix \( \langle b_t \rangle = 3 \) and \( \langle b_j \rangle = 2 \) for each interloper \( j \) in what follows. In the case explored here, the important interlopers are at lower redshift than the target line galaxies and so one expects the interlopers to be less clustered. This should be the case unless the interloper galaxies live in especially massive halos. In some other applications of our method, the interlopers may instead be mostly at higher redshift than the target line emitters. In this case, the interlopers would likely have a higher bias factor than the target line emitters. This would go in the direction of making the interloper emission harder to clean, but this should be offset in part by the smaller linear growth factor at high redshift. In any case, the impact of the interlopers will depend also on their average specific intensities relative to that in the target line.

In order to determine plausible values for the average specific intensity and shot-noise terms, we seek guidance from empirical correlations between the luminosity in the emission lines of interest and galactic star formation rates. These correlations can be combined with Schechter function fits to the abundance of galaxies as a function of their star formation rate to estimate the remaining quantities of interest, as in Pullen et al. (2013). The Schechter form for the star formation rate function is (Schechter 1976)

\[
\phi(\text{SFR})d\text{SFR} = \phi_* \frac{\text{SFR}_*^{\alpha}}{\text{SFR}_*} \exp\left(-\frac{\text{SFR}}{\text{SFR}_*}\right) d\text{SFR},
\]

with \( \alpha \) denoting the faint-end slope, and \( \phi_* \) and \( \text{SFR}_* \) giving, respectively, the characteristic star formation rate and number density.

The average specific intensity in each line can be estimated from the co-moving emissivity in the line according to (Lidz et al. 2011; Pullen et al. 2013):

\[
\langle I_t \rangle = \frac{\epsilon_L}{4\pi \nu_{\text{rest,L}} H(z)},
\]

where \( \nu_{\text{rest,L}} \) is the restframe emission frequency, \( \epsilon_L \) is the co-moving emissivity of the line emission, and the line profile has been approximated as a delta function in frequency. We further approximate the luminosity as a linear function of the star formation rate

\[
L = L_0 \frac{\text{SFR}}{M_\odot \text{yr}^{-1}}.
\]

Using the Schechter form for the star formation rate function, it follows that the co-moving emissivity in each line \( L \) is (Pullen et al. 2013):

\[
\epsilon_L = \phi_* L_0 \frac{\text{SFR}_*}{1 M_\odot \text{yr}^{-1}} \Gamma(2 + \alpha).
\]

We adopt the values of \( L_0 = 6 \times 10^6 L_\odot \) and the luminosity of the CO transitions given in Visbal & Loeb (2010) (see also Righi et al. 2008). For reference, \( L_{\text{CO}}^{(3-2)} = 7.0 \times 10^4 L_\odot \), while nearby higher-order rotational transitions have slightly higher luminosities until the luminosity declines again above CO(7-6). The CO luminosities are based on correlations between the strength of these emission lines and galactic star formation rates, as measured at low redshift, while the \([C\,\text{n}]\) luminosity-SFR relation is normalized to M82. Using the SFR functions from Smit et al. (2012) (adopting their nearest redshift bin for each interloper redshift), we can then estimate the emissivity and average specific intensity according to Equations (13)–(16). This gives \( \langle I_t \rangle = 5.7 \times 10^2 \text{Jy str}^{-1} \) for \([C\,\text{n}]\) emission at \( z = 7 \). Likewise, summing over interloper transitions, we find a combined average interloper intensity of \( \langle I_{\text{combined}} \rangle = 7.0 \times 10^2 \text{Jy str}^{-1} \), after including all non-negligible CO lines. Interestingly, the interloper and target contributions are comparable and so it will indeed be important to disentangle these two contributions. The top panel of Figure 2 gives further information, quantifying which interloper lines contribute most prominently to the total average intensity. According to our estimate, several distinct lines contribute significantly with the CO(4-3) at \( z = 0.88 \), CO(5-4) at \( z = 1.4 \), CO(6-5) at \( z = 1.8 \), and CO(7-6) at \( z = 2.3 \) transitions each contributing more than 10% \text{Jy str}^{-1}. While these simple estimates provide a useful guide, we caution that they adopt simplistic assumptions about the relationship between star formation and luminosity, and extrapolate empirical correlations beyond the redshifts at which they have been determined. (See also the discussion in the beginning of this section.) Our results are nevertheless broadly consistent with previous estimates in Silva et al. (2015), but differ in the details of the modelling and the empirical constraints adopted. Given the uncertainties in the signal and interloper strengths, we aim to devise a flexible approach for separating the interloper and target emission signals.

We also checked the impact of interloper emission from additional fine structure lines: \([C\,\text{i}] \) 610 \( \mu \text{m} \) at \( z = 1.1 \), \([C\,\text{i}] \) 371 \( \mu \text{m} \) at \( z = 2.4 \), \([N\,\text{i}] \) 205 \( \mu \text{m} \) at \( z = 5.2 \), and \([O\,\text{i}] \) 145 \( \mu \text{m} \) at \( z = 7.7 \). In our model, the strongest of these lines is \([C\,\text{i}] \) 371 \( \mu \text{m} \) which has an average specific intensity of \( \langle I_{\text{c,371\,\mu m}} \rangle = 54 \text{Jy str}^{-1} \), so it contributes less than 10% of the target emission. As justified further in the next paragraph, we neglect these potential interlopers in this work.

In order to quantify the relative importance of the interloper transitions to the power spectrum of intensity fluctuations, which is ultimately the signal we are after, we need to consider more than just the average specific intensity. Equations (12) and (10) imply that the relative strengths of the fluctuations depend mostly—aside for the shifting of power in wavenumber—on \( P_j \propto \langle b_j \rangle^2 \langle I_j \rangle^2 D^2(z_j)/(\alpha(z_j)\Gamma(2 + \alpha)) \), with \( D(z_j) \) being the linear growth factor at redshift \( z_j \). This applies on large scales where shot-noise contributions are negligible. We plot the relative strength of fluctuations, as characterized by this one number, in the bottom panel of Figure 2. In comparison with the average specific intensity, this number is enhanced for the lower \( J \) transitions because the distortion factor \( 1/(\alpha(z_j)\Gamma(2 + \alpha)) \) and the growth factor \( D(z_j) \) increase toward lower redshift. For the power spectrum of fluctuations, the dominant emission comes from the CO(4-3) line in this model, and the fluctuations in this line are more than a factor of two larger than in the target \([C\,\text{n}]\) line. Fluctuations from CO(3-2), CO(5-4), and CO(6-5) each contribute between 5% and 20% of the total interloper fluctuations. Higher-order transitions contribute less than several percent to the interloper fluctuations, and we will

\footnote{The latter line is at slightly higher redshift than the target line, and so might instead be referred to as an “extraloper” line.}
In addition to the clustering term, we should also consider the shot-noise contribution to the power spectrum from the target and interloper lines. This contribution may also be estimated from the \(L\)-SFR correlation, and the observed SFR Schechter function fits. Specifically, we expect the shot-noise from galaxies emitting in line \(L\) to be (e.g., Uzgil et al. 2014)

\[
P_{\text{shot},L} = \frac{(d_L)^2}{\phi_\ast} \frac{2 + \alpha}{\Gamma(2 + \alpha)}.
\]

Using the numbers from Smit et al. (2012) for \(\phi_\ast\) and \(\alpha\), we find \(P_{\text{shot},L} = 2.9 \times 10^5\text{ Jy}^2\text{str}^{-2}\text{ (Mpc/h)}^3\) for the target emission line. Summing over all of the interlopers, up to and including the CO(6-5) transition gives \(P_{\text{shot},\text{combined}} = 1.2 \times 10^7\text{ Jy}^2\text{str}^{-2}\text{ (Mpc/h)}^3\), after including the distortion factors. The shot noise from the interlopers is hence almost 50 times that in the target emission. In this work, we will consider the combined target plus interloper shot-noise as a single “nuisance” term that we aim to subtract out.

### 3.2. Apparent Interloper and Signal Power Spectra

We now turn to examine the model signal and interloper power spectra. As a first convenient way of characterizing the target and interloper power spectra, we expand the spectra in terms of Legendre polynomials and calculate the monopole and quadropole moments. The quadropole-to-monopole ratio may be written as

\[
Q(k) = \frac{5}{7} \int_{-1}^{1} d\mu [3\mu^2/2 - 1/2]P(k, \mu) \int_{-1}^{1} d\mu P(k, \mu).
\]

We can calculate the intrinsic target quadropole to monopole ratio, as well as that for the apparent interloper power spectra, incorporating the distortions as described by Equations (8)–(12).

The spherically averaged (monopole) power spectra are shown in the top panel of Figure 3. The solid black line shows the target \([C\,\text{ii}]\) emission power spectrum at \(z_j = 7\), \(k_b^2P_b(k)/(2\pi^2)\). In this model, the \([C\,\text{ii}]\) power spectrum has a strength of about \(\Delta^2 \approx 10^2\text{ Jy}^2\text{str}^{-2}\) at \(k \sim 0.01\text{ h Mpc}^{-1}\), \(\Delta^2 \approx 3 \times 10^3\text{ Jy}^2\text{str}^{-2}\) at \(k \sim 1\text{ h Mpc}^{-1}\), and reaches \(\Delta^2 \approx 1.5 \times 10^7\text{ Jy}^2\text{str}^{-2}\) at \(k \sim 10\text{ h Mpc}^{-1}\). The clustering term dominates on large scales at \(k \lesssim 3\text{ h Mpc}^{-1}\) or so, while the shot-noise term is more important on smaller scales. The blue-dashed and red-dotted lines show the interloper contamination power, with and without coordinate distortions, respectively. For each interloper line, the coordinate distortions shift power from \(k_j \rightarrow k_j/\alpha(z_j)\) and from \(k_j \rightarrow k_j/\alpha_\ast(z_j)\), while boosting the fluctuation power by the overall \(1/(\alpha(z_j)\alpha_\ast(z_j))\) factor. After spherical averaging, this leads to a shift and boost in the apparent interloper power, as may be discerned by comparing the blue dashed and red dotted lines in Figure 3. As anticipated in the previous section, the combined CO interloper power exceeds the target \([C\,\text{ii}]\) emission power by a factor of several on large scales—the precise excess depends on scale because of the coordinate distortions—and so it is crucial to remove this contamination. On smaller scales the target and interloper power differ because of the larger Poisson noise from the interloper populations: we expect the interloper shot-noise to swamp that in the \([C\,\text{ii}]\) target emission. The larger interloper shot-noise mostly results because star

![Figure 2. Relative importance of interloper lines to the average specific intensity and to the power spectrum of intensity fluctuations. Top: the estimated intensity of different interloper transitions, CO(1 \rightarrow 0) as a function of \(J\), relative to the model \([C\,\text{ii}]\) target emission intensity. Bottom: the \(y\)-axis shows a factor that determines the relative contribution of different interloper lines to the total power spectrum of intensity fluctuations (see the text). The normalization has been set here so that the factor sums (over all lines) to unity. The black horizontal line shows the same factor for the target line, \([C\,\text{ii}]\) at \(z = 7\).](image)
formation occurs in lower mass, yet more abundant systems at high redshift and so the Poisson noise in the high-redshift target line is relatively low. As mentioned previously, in this work we will be content to extract only the [C\textsc{ii}] clustering term and forego trying to separate out the [C\textsc{ii}] shot-noise term in the presence of this large interloper contamination.

Although the shape of the target and interloper monopole power differ only subtly, the angular dependence of the target and interloper power is quite different. For example, the bottom panel of Figure 3 shows the quadropole to monopole ratio for both the target and interloper emission power spectra. For illustration, we show the CO interloper quadropole to monopole ratio both with and without coordinate mapping distortions. The quadropole to monopole ratio for the target emission, and the interloper emission without coordinate mapping distortions, have the usual form expected from redshift space distortions. On sufficiently large scales, \( Q \rightarrow (4.3^3 + 4.3^2/7)/(1 + 2.3^3 + 3^2/5) \) — the Kaiser effect result (Kaiser 1987) — while the quadropole anisotropy diminishes on smaller scales owing to the finger-of-god effect and the isotropic shot-noise term. The intrinsic interloper \( Q(k) \) turns over on larger scales (smaller \( k \)) than the target \( Q(k) \) because the interloper shot-noise term is bigger and because the finger-of-god suppression is stronger at the (lower) redshifts of the interloper lines. The blue dashed line shows the quadropole to monopole ratio after incorporating the coordinate mapping distortion. This reaches much larger values than expected from the Kaiser effect, with the model \( Q \) peaking near \( Q = 2.6 \) at \( k = 0.2h \text{ Mpc}^{-1} \) before gradually turning over on smaller scales owing to the finger-of-god effect and shot-noise. This is a direct consequence of the difference between the mapping factors, \( \alpha_i(z) \) and \( \alpha_t(z) \), and the shape of the linear power spectrum of density fluctuations. The increasing \( Q(k) \) from \( k \sim 0.01 \) to \( 1h \text{ Mpc}^{-1} \) reflects the steepening of the power spectrum spectral index toward small scales. This can be verified by calculating the quadropole to monopole ratio for a pure power law power spectrum (of varying spectral index) under the coordinate warping transformation. The steeper \( k \) dependence at small scales enhances the difference between the line of sight and transverse power after applying the warping. Note that on scales larger than the co-moving horizon size at matter radiation equality, \( k \leq k_{\text{eq}} \approx 0.015h \text{ Mpc}^{-1} \), the net interloper distortion is sub-Kaiser because the linear matter power spectrum is an increasing function of \( k \) on these scales.

In order to further characterize and visualize the target and interloper power spectrum anisotropies, we plot contours of constant power in the \( k_{\parallel} - k_{\perp} \) plane (Figure 4 see also Gong et al. 2014). The top panel illustrates the redshift space distortion in the target emission. As mentioned earlier, if the large-scale anisotropy shown here can be measured accurately, we can determine the luminosity-weighted bias of the emitters in the target line (from the dependence on \( \beta_i \)), as well as the average specific intensity of the target emission (from the overall amplitude of fluctuations). The contours in the bottom panel show a strong elongation in the \( k_{\parallel} \) direction from the coordinate mapping distortion, which sources the strong quadrupole moment shown in Figure 3 as discussed previously. Note that the total interloper power spectrum in our model is the sum of four separate interloper lines from different redshifts, CO(3-2) at \( z = 0.407 \), CO(4-3) at \( z = 0.877 \), CO(5-4) at \( z = 1.35 \), CO(6-5) at \( z = 1.82 \). The total anisotropy of the interloper emission, illustrated in Figures 3 and 4 hence reflects a weighted average of these four interloper lines, with the CO(4-3) line having the strongest weight in our model (see the bottom panel of Figure 2).
The interloper contamination. Here, we instead consider fitting the full angular dependent power spectrum using parameterized models.

4. FORECASTS

Having quantified the power spectrum anisotropy, we now forecast the prospects for using this to separate out the interloper and target contributions to the power spectrum. Here, we assume that Equations (9)–(12) provide a perfect description of the measured power spectra. We then investigate how well the parameters of the model may be determined by hypothetical $[\text{C} \text{II}]$ surveys. The shortcoming of this approach is that it relies on simple models for the power spectra of intensity fluctuations, which may be imperfect. In future work, it will be important to develop consistency checks of this model, and/or to develop a more sophisticated description. We discuss some possible observational tests in Sections 5 and 6.

In general, we consider a seven-dimensional parameter space described by a vector, $\mathbf{q}$, with seven components: $\{q_1, q_2, \ldots, q_7\} = \{\langle l_1 \rangle, \langle b_1 \rangle, \langle l_2 \rangle, \langle b_2 \rangle, \langle l_3 \rangle, \langle b_3 \rangle, \langle b_{\text{tot}} \rangle\}$. The parameters describe the specific intensity of the target emission, the average bias of this emission, the specific intensity of each of the four important interloper lines (indexed by the rotational states of the CO transitions with $J, J = 1$ as subscripts: e.g., $\langle l_2 \rangle$ is the average specific intensity in the $J = 3 \rightarrow 2$ transition), and the total (target plus all interlopers) shot-noise. Here, we implicitly fix the bias of the fluctuations in each interloper line to $\langle b_i \rangle = 2$. Since the interloper power is determined mostly by the overall product of specific intensity and bias (aside for the additional dependence on $\beta$ through the Kaiser effect which is small relative to the anisotropy induced by assuming an incorrect redshift), one can think of the specific intensity constraints derived as confidence intervals on the product $\langle b_j \rangle \langle l_j \rangle$.

Our main goal then is to determine whether the target emission fluctuations, characterized by the parameters $\langle l_j \rangle$ and $\langle b_j \rangle$, may be determined accurately in the presence of the interloper fluctuations. We investigate this by calculating Fisher matrices for futurionic $[\text{C} \text{II}]$ surveys. The components of the Fisher matrix for parameters $q_i$ and $q_j$ are given by

$$F_{ij} = \int_{\vartheta_{\text{min}}}^{\vartheta_{\text{max}}} d\mu \times \int_{k_{\text{min}}}^{k_{\text{max}}} \frac{d k k^2 V_i}{4\pi^2} \frac{\partial P(k, \mu)}{\partial q_j} \frac{\partial P(k, \mu)}{\partial q_i} \frac{1}{\text{var}[P(k, \mu)]}.$$  \hspace{1cm} (19)

where we have approximated the discrete sum over modes in the survey by a continuous integral. Here the integral over angle runs over the upper half-plane, between some ($k$-dependent) limits $k_{\text{min}}$ and $k_{\text{max}}$ that we will describe below, and the integral over wavenumber ranges between the limits $k_{\text{min}}$ and $k_{\text{max}}$. The quantity $V_i$ is the co-moving volume of the survey. This expression depends on that variance of the total power spectrum of fluctuations for each $k$-mode, $\text{var}[P(k, \mu)]$.

We compute this, neglecting non-Gaussian contributions to the variance, as:

$$\text{var}[P(k, \mu)] = [P_{\text{tot}}(k, \mu) + P_N(k, \mu)]^2.$$  \hspace{1cm} (20)

Here, $P_{\text{tot}}(k, \mu)$ is the total signal plus interloper emission power spectrum, including the shot-noise contribution, and $P_N(k, \mu)$ is the detector noise power spectrum.
It is also instructive to consider the number of Fourier modes in the upper-half plane in a bin of \( k \) and \( \mu \), \( N_m(k) \). For a survey of co-moving volume \( V_s \), the number of modes contained within the survey volume in a wavenumber bin of thickness \( \Delta \ln(k) \Delta \mu \) is

\[
N_m(k) = \frac{k^3 V_s}{4\pi^2} \Delta \ln(k) \Delta \mu.
\] (21)

Note that this is just included for illustration, since the mode-counting is already handled implicitly in the Fisher matrix calculation (Equation (19)).

### 4.1. Survey Parameters

It will be challenging to measure the power spectrum and its angular dependence precisely enough to separate the faint interloper and target signals using this methodology. Nevertheless, experiments are already underway to detect the reionization-era [C II] signal (e.g., the TIME-Pilot experiment, Crites et al. 2014); we anticipate that the sensitivity of these measurements will increase rapidly, fueled by advances in detector technology. As a convenient baseline, we consider the “CII-Stage II” survey described in Silva et al. (2015). Unfortunately, we find that even this is less sensitive than we require, so we generally consider a still more sensitive experiment, as specified subsequently.

Our baseline survey is described in Silva et al. (2015) and consists of a single 10 m dish, with 16,000 bolometers and an \( N_{\text{sp}} = 64 \)-beam spectrometer with a frequency resolution of \( \Delta \nu = 0.4 \text{ GHz} \). The hypothetical survey spans 100 deg\(^2\) on the sky for a total observing time of \( t_{\text{survey}} = 2000 \text{ hr} \). We consider a \( B = 20 \text{ GHz} \) bandwidth of observations near \( z = 7 \), which is small enough for us to neglect evolution in the signal across the survey bandwidth. The angular resolution of the survey is \( \Delta \theta = 0.43 \text{ arcminutes} \). In co-moving coordinates, the pixels span \( x_{\text{pix,res}} = 0.790 \text{ Mpc/h} \) in the transverse direction and \( x_{\text{pix,res}} = 3.42 \text{ Mpc/h} \) in the line of sight direction. In the line of sight direction, the survey length is \( L_{\|} = 171 \text{ Mpc/h} \), while the transverse dimension is \( L_{\perp} = 1.09 \times 10^3 \text{ Mpc/h} \). The total survey volume is \( V_s = 2 \times 10^8 \text{ (Mpc/h)}^3 \). For reference, the number of modes surveyed is \( N_{\text{sp}}(k) = 5.2 \times 10^3 (k/0.1 \text{ h Mpc}^{-1})^3 \Delta \ln(k) \Delta \mu \) in a bin around \( k = 0.1 \text{ h Mpc}^{-1} \).

The survey noise power spectrum may be written as (e.g., Uzgil et al. 2014)

\[
P_N(k_{||}, k_{\perp}) = \frac{\sigma_N^2}{t_{\text{obs}}} V_{\text{pix}} e^{(k_{||}x_{\text{pix,res}})^2 + (k_{\perp}x_{\text{pix,res}})^2},
\] (22)

where \( \sigma_N^2/t_{\text{obs}} \) is the noise per pixel in specific intensity units (squared), \( V_{\text{pix}} \) is the pixel volume, and the exponential factor accounts for the finite angular and spectral resolution of the instrument. We can extract plausible numbers for the noise power spectrum from Table 8 of Silva et al. (2015), converting from the Noise Equivalent Flux Density (NEFD) to the specific intensity noise (\( \times \)square-root of time in seconds), using \( \sigma_N = \text{NEFD}/(\Delta \Omega_{\text{pix}}) \). Note also that the observing time per pixel is \( t_{\text{obs}} = t_{\text{survey}} N_{\text{sp}} \Delta \Omega_{\text{pix}}/\Delta \Omega_{\text{survey}} \), where \( N_{\text{sp}} \) is the number of spatial pixels and \( t_{\text{survey}} \) is the total survey observing time.

This resulting noise power spectrum is

\[
\frac{\sigma_N^2}{t_{\text{obs}}} V_{\text{pix}} = 8.7 \times 10^5 \text{ Jy}^2 \text{ str}^{-2} (\text{ Mpc/h})^3 \left[ \frac{\sigma_N}{\text{Jy/str} \sqrt{h}} \right]^2 \times \left[ \frac{V_{\text{pix}}}{2.13 \text{ (Mpc/h)}^2} \right] \left[ \frac{64}{N_{\text{sp}}} \frac{2000 \text{ hr}}{t_{\text{survey}}} \right].
\] (23)

Since we find that even this sensitivity is insufficient for our purposes, we consider a still more sensitive experiment with \( \frac{\sigma_N^2}{t_{\text{obs}}} V_{\text{pix}} = 4.3 \times 10^5 \text{ Jy}^2 \text{ str}^{-2} (\text{ Mpc/h})^3 \). This value represents our fiducial noise level in what follows. We caution that the noise power here is approximately twenty times smaller than in the stage II experiment considered by Silva et al. (2015), so the rms noise in our fiducial case is four to five times smaller than in their work. Naturally, it will be important to see if this sensitivity is in fact achievable. Improvements may be possible by going to space, in which case the CMB would set the photon background noise rather than emission from the Earth’s atmosphere. Rapid progress in detector development may also help to increase sensitivity beyond what is assumed here, e.g., it may be possible to increase the number of spatial pixels, \( N_{\text{sp}} \). We will describe how the results depend on this somewhat arbitrary choice of noise power.

It may also be possible to make progress with noisier survey data by masking bright pixels suspected of containing CO interloper emission, while using the anisotropy of the residual fluctuation power spectrum to further clean interloper contamination. In other words, the masking approach advocated in previous work may be combined with the technique developed here. Further work is required to explore whether the two techniques may indeed be combined fruitfully. If one masks pixels suspected of interloper contamination, this should reduce the interloper fluctuation power and make it harder to fit-out interloper contributions. Nevertheless, applying our approach after masking might provide a valuable cross-check: if distinctive anisotropic emission remains, this suggests residual interloper contamination. We expect this combination of techniques to be most valuable in the case that the interloper contamination is stronger than assumed here. Finally, there may be some benefit to a sparse-sampling survey strategy to build up a large field of view quickly—rather than mapping contiguous regions on the sky—although this will lead to aliasing from high-\( k \) modes (Kaiser 1998; Chiang et al. 2013).

We are almost ready to calculate the Fisher matrix elements using Equation (19), but we need to comment first on one additional complication. The issue relates to the continuum foreground, which is significantly larger than the line interloper emission. The continuum emission at the frequencies of interest is dominated by the Cosmic Infrared Background (CIB), produced by dust grains in galaxies at a range of redshifts, and has an average specific intensity of \( \sim 1 \times 10^4 \text{ Jy str}^{-1} \) (Silva et al. 2015). Although this is two to three orders of magnitude larger than the expected [C II] emission, the continuum foreground should nevertheless be separable using the fact that it is spectrally smooth, i.e., one can use exactly the same strategy as advocated for cleaning foregrounds from redshifted 21 cm fluctuation measurements (e.g. Zaldarriaga et al. 2004). In order to separate the spectrally smooth foreground, however, one inevitably sacrifices measuring long
wavelength modes along the line of sight. Additional modes will likely be lost as well, since the frequency dependence of the beam, calibration errors, and instrument imperfections can also produce spurious spectral structure in the foregrounds, as observed by the instrument. Here we will ignore this “mode-mixing” problem (e.g., Liu & Tegmark 2011; Ali et al. 2015), and take a simplistic approach: we simply remove line-of-sight modes with wavelength smaller than the bandwidth of the measurement, i.e., modes with line-of-sight wavenumber smaller than \( k_{\parallel,\min} = 2\pi/Q_1 = 0.037h^{-1}\) Mpc\(^{-1}\). Further work is required to determine whether measuring the angular dependence of the power spectrum is feasible in the presence of realistic levels of mode-mixing. Mode-mixing should be significantly less worse here than in the case of 21 cm; this is in part because the continuum to line emission ratio is smaller, and also because the instrumental beam is simpler for this single dish experiment.

Before exploring forecasts for marginalized constraints on the parameters \( q \), it is instructive to explicitly examine some of the derivatives that enter the Fisher matrix calculation of Equation (19). Figure 5 compares the derivatives of the total power spectrum with respect to each of the specific intensity parameters as a function of angle, \( \mu \), for fixed \( k = 0.5h\) Mpc\(^{-1}\). The range of \( \mu \) accessible is limited slightly by removing the spectrally smooth modes with \( k_1 \leq 2\pi/Q_1 \) to \( \mu \geq \mu_{\min} = k_{\parallel,\min}/k = 0.074 \) for \( k = 0.5h\) Mpc\(^{-1}\). Derivatives with respect to the interloper line intensities show a steeper angular dependence than the target emission, as expected. This is because the interlopers are subject to the coordinate distortion, while the target line depends on angle primarily through the Kaiser effect (at the wavenumber considered, the finger of god effect is sub-dominant). A simple way to understand the angular dependence of the interloper power is to note that, approximating the power spectrum at the wavenumber of interest by a power-law of spectral index \( k^{-n_{eff}} \), the ratio of the power at \( \mu = 1 \) to that at \( \mu = 0 \) is simply \( (\alpha_1(z_f)/\alpha_0(z_f))^{n_{eff}} \). This rough estimate ignores the Kaiser effect, which will further enhance this ratio. For \( k = 0.5h\) Mpc\(^{-1}\), \( n_{eff} = -d\ln P/d\ln k = 2.1, \) and this ratio is 110 for the strongest case of the CO(3-2) interloper distortion. The derivative shown is proportional to the square of this number and so the ratio reaches four orders of magnitude, and the result in Figure 5 is still slightly larger because it includes the Kaiser distortion.

In any case, Figure 5 further motivates that the angular dependence of the derivatives with respect to the intensity in the various lines gives some sense for which lines will be most degenerate with each other. For example, the weaker angular dependence of the target line derivative suggests that \( \langle l_i \rangle \) should not be strongly degenerate with the intensities in the interloper lines, provided the full angular range shown is well-measured. This should be especially so in comparison to the low-order transitions that show the strongest angular variation. On the other hand, we expect the intensity in the CO(4-3) and CO(5-4) lines to be more degenerate given their relatively similar redshifts and distortion factors.

We now turn to calculate the Fisher matrix of Equation (19), and invert this matrix to find the constraints on the various parameters. We first consider the constraints on the target signal, contrasting the results for the stage II survey with noise power at the level of Equation (23) and a sample-variance (also known as “cosmic-variance”) limited survey, with negligibly small noise power, over the same volume. The top panel of Figure 6 shows the projected errors in the \( \langle l_i \rangle - \langle b_i \rangle \) plane, marginalized over the interloper parameters. The contours show that the hypothetical sample-variance limited survey is capable of constraining \( \langle l_i \rangle \) and \( \langle b_i \rangle \), even in the presence of strong interloper contamination. Quantitatively, we forecast \( \sim 3\% \) level \( 1 - \sigma \) marginalized constraints on these parameters in the sample variance limit. The ellipse shows the expected strong degeneracy between increasing \( \langle l_i \rangle \) and decreasing \( \langle b_i \rangle \); nevertheless, the Kaiser effect allows separate constraints on the two parameters although they are highly correlated. However, it is hard to achieve the requisite sensitivity given the bright night sky at these frequencies. If we instead incorporate noise at the level of Equation (23), the marginalized errors blow up considerably, as illustrated by the bottom panel of Figure 6. In this case the marginalized constraints on the average specific intensity and the bias only give \( 1 - \sigma \) detections—i.e., without attempting to mask interloper emission, a significant detection is not possible for this survey.

For now, we simply consider a more sensitive experiment with \( (\sigma^2_N V_{\text{pix}})/I_{\text{obs}} = 4.3 \times 10^5 \text{Jy}^2 \text{str}^{-2}(\text{Mpc}/h)^3 \). The \( \langle l_i \rangle - \langle b_i \rangle \) results, marginalized over the interloper parameters, are shown for this level of noise in Figure 7. Unless otherwise noted, we adopt this value for the noise power spectrum in what follows. In this case, 20% level constraints on the target emission parameters are achievable (at \( 1 - \sigma \)) and the target and interloper emission fluctuations can indeed be separated.

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Figure 5. Derivatives with respect to average specific intensity in different lines as a function of angle. Here, the power spectrum derivatives are computed for \( k = 0.5h\) Mpc\(^{-1}\). The derivatives are much stronger functions of angle for the interloper line—owing to the coordinate distortions—than for the target [C ii] emission, which depends on angle only through the Kaiser effect. The low-order CO transitions show a stronger dependence on angle because their coordinate distortions are larger.
The $C\text{II}$ emission signal at $z \sim 7$ may also be stronger than in the model considered here, which could relax the stringent requirements on the noise power spectrum found here. Indeed, as we were finalizing this manuscript we learned of similar work by Y.-T. Cheng & T.-C. Chang (2016, in preparation). These authors’ model gives a $z = 6$ [C\text{II}] emission signal that is more than an order of magnitude larger than our $z = 7$ predictions, and so they are more optimistic about the prospects of applying this method using upcoming datasets. For the most part, the difference stems from the larger bias factor in their model, with $b_2$ almost six times as large as in our calculations. Their bias factor comes from relating the line luminosity to the CIB and from empirically calibrated models connecting CIB luminosity and halo mass. Since most of the CIB emission comes from lower redshift, the $z = 6$–7 predictions are still uncertain, however. In any case, this further illustrates the uncertainties in forecasting the expected signal. Improved constraints on the relationships between line-luminosity, star formation rate, and halo mass, will be needed to refine our predictions for the target and interloper emission fluctuations.

It is also helpful to examine the constraints on the interloper emission parameters. Some example confidence intervals are shown in Figure 8. The left hand panel shows the joint forecasted constraints in the $\langle I_i \rangle - \langle b_i \rangle$ plane. Evidently, the target fluctuations can be extracted using the angular dependence of the emission power spectrum but greater sensitivity is required than in the hypothetical stage-II survey. Note that we allow regions in parameter space where the parameters are negative. In practice, one might invoke a prior to exclude such regions as unphysical.

The [C\text{II}] emission signal at $z \sim 7$ may also be stronger than in the model considered here, which could relax the stringent requirements on the noise power spectrum found here. Indeed, as we were finalizing this manuscript we learned of similar

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Figure 6. Forecast of constraints in the $\langle I_i \rangle - \langle b_i \rangle$ plane, marginalized over the interloper contamination and shot-noise parameters for two noise levels. Note that the range of values shown along the $x$ and $y$-axes differ significantly between the two panels. The red, blue, and green contours show 1, 2, and 3 $\sigma$ confidence intervals, respectively, while the “x” marks the assumed central value. (The contours and “x”s have the same meaning in subsequent plots.) The specific intensity, $\langle I_i \rangle$, has been expressed in units of our fiducial model value, $\langle I_i \rangle = 5.7 \times 10^{3}$ Jy sr$^{-1}$. Top: in this case, a sample-variance limited experiment is shown, i.e., the noise power spectrum is taken to be negligibly small. Bottom: here the noise power spectrum instead follows Equation (23), as expected for the “stage-II” [C\text{II}] survey. Evidently, the target fluctuations can be extracted using the angular dependence of the emission power spectrum but greater sensitivity is required than in the hypothetical stage-II survey. Note that we allow regions in parameter space where the parameters are negative. In practice, one might invoke a prior to exclude such regions as unphysical.

Figure 7. Forecast of constraints in the $\langle I_i \rangle - \langle b_i \rangle$ plane, marginalized over the interloper contamination and shot-noise parameters for our fiducial noise power spectrum. Identical to Figure 6, except for our fiducial noise level (see the text).

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3 Thanks to the “Opportunities and Challenges in IM Workshop” held at Stanford.
Figure 8. Forecasted constraints on the average specific intensity of two of the interloper emission lines. Top: constraints in the \((I_{\text{CO}})-I_{\text{CO}(4-3)})\) plane. The fractional error is larger for the interloper emission than for the target emission. This is because the average specific intensity of the target line is larger, and because the intensity of this interloper line is highly degenerate with that of other interloper lines. Bottom: constraints in the \(I_{\text{CO}(4-3)}-I_{\text{CO}(5-4)})\) plane. The constraint ellipses show a strong degeneracy, since increasing the strength of one interloper line may be mostly compensated by reducing the strength of another line. As in Figure 6, we allow unphysical regions where the parameters are negative.

\(\alpha_1\) and \(\alpha_2\), and their power spectra hence show almost the same angular dependence. For example, the right-hand panel of Figure 8 gives confidence intervals in the \(I_{\text{CO}(4-3)}-I_{\text{CO}(5-4)})\) plane, and this reveals the expected strong anti-correlation between the emission in these two lines. Quantitatively, the correlation coefficient in this plane is \(\rho = -0.81\). After marginalizing over all of the interloper parameters, the error bars on the average intensity of each interloper line are large: in our fiducial case, we only expect a greater than \(2 - 3 - \sigma\) detection of \(I_{\text{CO}(4-3)}\), even though we obtain a significant detection \((\geq 5 - \sigma)\) of the \([\text{C}\,\text{II}]\) target emission line. For reference, our fiducial survey numbers forecast detections of the specific intensity in the \(\text{CO}(3-2)\) and \(\text{CO}(5-4)\) lines at only slightly better than \(1 - \sigma\), while the \(\text{CO}(6-5)\) specific intensity is still less detectable.

In summary, the angular dependence of the emission fluctuations can be used to separate the target and interloper emission fluctuations if the noise power spectrum is sufficiently small. Since the main goal is to extract information about the target \([\text{C}\,\text{II}]\) emission, perhaps it is not a big concern that the individual CO interlopers are themselves somewhat degenerate, and the constraints on these parameters are weaker. However, further checks seem valuable given that our approach relies on having a good model for each source of emission fluctuations.

5. CROSS-CORRELATING WITH LSS TRACERS

Fortunately, there are other approaches we can pursue as further cross checks on the analysis of the previous section, some of which should enable separate constraints on each interloper line. First, we can correlate the IM data cubes with spectroscopic galaxy and/or quasar catalogs at the interloper redshift (Silva et al. 2015). We expect that by the time \([\text{C}\,\text{II}]\) IM experiments are underway, there will be other extensive large-scale structure surveys, spanning large fields of view and overlapping in redshift with the prominent CO interloper transitions. We can use cross-correlations with LSS tracers at different redshifts to separately constrain the parameters of each of the various CO interloper lines.

For instance, consider the cross power spectrum between interloper line \(j\) and the abundance of spectroscopic galaxies at the same redshift, \(z_j\). Suppose the average bias of these tracer galaxies is \(\langle b\rangle\). In order to extract the cross spectrum of interest, it is convenient to convert from angles and wavelengths to co-moving units assuming the interloper redshift \(z_j\), rather than the target \([\text{C}\,\text{II}]\) redshift, \(z\). The target line and the other interloper lines will not contribute on average to the cross spectrum with the LSS tracer at \(z\) since these lines originate at significantly different redshifts, but they will contribute to the variance of the cross spectrum, as we will describe. For this purpose, the total power spectrum of intensity fluctuations from line emission is computed along the lines of Equation (9), except that the warping is now relative to the coordinates of an interloper at redshift \(z_j\). The cross power spectrum with the galaxy tracer field is then

\[
P_{k}(k, \mu) = \langle I_j \rangle \langle b \rangle \langle b\rangle (1 + \beta_j \mu^2)(1 + \beta_{\text{gal}} \mu^2)
+ D_{\text{IM}} \kappa_{\text{gal}}(z) P_{k}(k, z_j),
\]

where \(\beta_j = f_j(z_j)/\langle b\rangle\) and \(\beta_{\text{gal}} = f_{\text{gal}}(z_j)/\langle b\rangle\) are the Kaiser parameters for the interloper line and the galaxy density field, respectively. We have assumed here that the finger-of-god suppression has an identical form for the IM galaxies and for the LSS tracer population at the same redshift; although this is unlikely true in detail, we expect this simplification to have little impact on our results. Here for simplicity we have also assumed that the CO emitting populations and the tracer galaxies are largely disparate populations; otherwise, there should be an additional shot-noise term in Equation (24). In any case, if the cross spectrum can be measured accurately.
enough we can infer constraints on \( \langle I_j \rangle \), \( \langle b_j \rangle \), and \( \langle b_{\text{gal}} \rangle \), or at least their overall product. One final caveat here, however, is that we have not included a stochasticity parameter “r” in the above equation and so we are implicitly assuming that the galaxies and interloper populations are perfect tracers of large-scale structures on the scales of interest for this measurement. In addition, the auto spectrum of the tracer galaxies may be used to measure \( \langle b_{\text{gal}} \rangle \). Ideally, future LSS surveys will provide tracer galaxy or quasar samples at the redshifts of each of the prominent CO interlopers. These measurements can then be combined with the angular dependence of the intensity auto spectrum, to further separate the interloper contaminants from the target emission fluctuations.

The variance (per mode) of the cross spectrum is given by

\[
\text{var}[P(k, \mu)] = \left[ P^2 + (P_{\text{gal}}(k, \mu) + P_{\text{N}}(k, \mu)) \times \left( P_{\text{gal}}(k, \mu) + \frac{1}{n_{\text{gal}}} \right) \right],
\]

(25)

where \( P_{\text{gal}}(k, \mu) \) is the total line intensity power spectrum, except computed here with the distortion factors considered relative to the coordinates at the interloper redshift \( z_i \). \( P_{\text{N}}(k, \mu) \) is the noise power spectrum for the IM survey (Equation (22)), while \( P_{\text{gal}} \) and \( 1/n_{\text{gal}} \) are the clustering and shot-noise terms for the tracer galaxies. After specifying the properties of our tracer galaxies and the survey parameters, the cross-spectrum Fisher matrix, \( F_{ij} \), may be computed along the lines of Equation (19):

\[
F_{ij} = \int_{\mu_{\text{max}}}^{\mu_{\text{min}}} d\mu \int_{\theta_{\text{min}}}^{\theta_{\text{max}}} \frac{d\theta_{\text{max}}^2V_i \partial P_{\text{c}}(k, \mu) \partial P_{\text{d}}(k, \mu)}{4\pi^2 \partial \theta_{ij} \partial \theta_{ij} \text{var}[P(k, \mu)]},
\]

(26)

Here, the parameter vector is specified by just three components: \( \theta = \{ \langle I_j \rangle, \langle b_j \rangle, \langle b_{\text{gal}} \rangle \} \).

As an example of the cleaning that may be feasible with future data sets, we consider surveys for narrow emission-line galaxies using the Dark Energy Spectroscopic Instrument (DESI) (Levi et al. 2013). We suppose that the entire volume of the IM survey is contained within the DESI narrow emission line galaxy survey, which is plausible given that DESI will cover a large-fraction of the full sky. In this case, the number of modes surveyed and the spatial and spectral resolution of the cross-spectrum measurement are entirely limited by the IM survey specifications and the only additional relevant parameters for our Fisher matrix forecasts are the tracer galaxy bias parameters (this fixes \( P_{\text{gal}}(k, \mu) \) in our linear biasing model), and the abundance \( n_{\text{gal}} \) which determines the shot-noise contribution to the variance for the DESI galaxies. We adopt the abundance of narrow-emission-line galaxies that may be observed by DESI as reported in Levi et al. (2013). In this case, near the redshift of the CO(4-3) interloper emission, we expect a number density of \( n_{\text{gal}} = 5.2 \times 10^{-4} h^3 \text{Mpc}^{-3} \). The expected abundance of DESI tracer galaxies at the redshifts of the other prominent interlopers are comparable. Finally, we would like to account for the constraint that will be possible on \( \langle b_{\text{gal}} \rangle \) from a measurement of the auto-spectrum of the tracer galaxy survey. Note that the DESI emission line galaxies will themselves suffer from interloper contamination (e.g., Pullen et al. 2016) and this will need to cleaned in order to measure the auto-spectrum and \( b_{\text{gal}} \). Rather than investigate this in detail here, for simplicity we suppose that \( b_{\text{gal}} \) is measured to 10% fractional accuracy. We believe this is conservative. This is then incorporated as a prior in the cross-spectrum Fisher matrix calculation (Equation (26)). For the bias of the tracer galaxies, we adopt a central value of \( b_{\text{gal}} = 2.5 \).

Figure 9 shows an example of the constraints that may be obtained for the case of CO(4-3) interloper line emission. Evidently, the cross spectrum with the DESI narrow emission line galaxy sample should allow significantly tighter constraints on \( \langle I_{\text{CO}(4-3)} \rangle \) than from the total IM auto spectrum. For our fiducial assumptions, the \( 1 - \sigma \) fractional error bar on \( \langle I_{\text{CO}(4-3)} \rangle \) improves by a factor of more than four. Similar measurements should be possible for each of the other CO interloper transitions. These cross-spectrum measurements should be useful both as a consistency check on the interloper modeling, and can be used in combination with the total IM auto spectrum to reduce error bars on the target emission parameters. Quantitatively, we can incorporate the DESI-like cross-spectrum constraints on the specific intensity of the interloper lines as \( 1 - \sigma \) priors in our auto-spectrum Fisher matrix calculations. Doing this, we find that the error bars on the \( [\text{C}\,\text{II}] \) specific intensity and bias shrink by a factor of 1.5 and 1.4 respectively. Although these numbers are indicative, the precise gain will depend on the noise power spectrum in the IM experiment and on how accurately the auto-spectra of the DESI galaxies are measured.

### 6. CROSS SPECTRUM WITH OTHER LINES

Finally, an additional approach to help confirm the presence of target \( [\text{C}\,\text{II}] \) emission fluctuations is to cross-correlate with a data cube centered on a different frequency that contains emission from another line at the same redshift (e.g., Visbal &
 Loeb 2010). Indeed, this measurement may potentially be done with the same data set. For example, the hypothetical [C\textsc{ii}] survey discussed in Silva et al. (2015) spans 200-300 GHz. In addition to the [C\textsc{ii}] 158 \mu m line at z = 7, the same survey should include [O\textsc{i}] emission at z = 7 with a rest frame wavelength of 146\mu m, at an observed frequency of \nu_{\text{obs}} = 259 GHz. Further, just outside the fiducial range spanned by this hypothetical survey is an [N\textsc{ii}] 122 \mu m emission line at z = 7, \nu_{\text{obs}} = 308 GHz. The cross spectrum between the [C\textsc{ii}] and [O\textsc{i}] data cubes, for example, should follow

\begin{equation}
\begin{split}
P_{\alpha,\text{C\textsc{ii}}-\text{O}\textsc{i}}(k, \mu) &= \langle l_i \rangle \langle l_{\text{O}\textsc{i}} \rangle \langle b_i \rangle \langle b_{\text{O}\textsc{i}} \rangle (1 + \beta / \mu)^2 (1 + \beta_{\text{O}\textsc{i}} \mu^2) \\
&\quad \times D[\mu k \sigma_p(z_i)] P_{\rho}(k, z_i) + P_{\text{shot, C\textsc{ii}}-\text{O}\textsc{i}},
\end{split}
\end{equation}

where \langle l_{\text{O}\textsc{i}} \rangle and \langle b_{\text{O}\textsc{i}} \rangle denote the specific intensity and linear bias factor of the [O\textsc{i}] emitters that lie at the same redshift as the [C\textsc{ii}] emission, and the other symbols have their usual meanings. Similar to Equation (24), we assume that the finger-of-god suppression has an identical form for each set of emitters. In what follows, we neglect the shot-noise term, \mathcal{P}_{\text{shot, C\textsc{ii}}-\text{O}\textsc{i}}. Strictly speaking, this is only correct in the limit that disparate populations of sources produce the [C\textsc{ii}] and [O\textsc{i}] emission. However our sensitivity here is coming from large scales where the shot-noise contribution should be small, so we do not expect neglecting it to impact our estimates.

Here, we consider using the cross spectrum between [C\textsc{ii}] and [O\textsc{i}] as a test of the high-redshift origin of a potential [C\textsc{ii}] contribution to the IM data cube. For this purpose, we define

\begin{equation}
A = \langle l_i \rangle \langle l_{\text{O}\textsc{i}} \rangle \langle b_i \rangle \langle b_{\text{O}\textsc{i}} \rangle and consider the significance at which A can be shown to be non-zero. Here, the relevant variance is
\begin{equation}
\begin{split}
\text{var}\{P_{\alpha,\text{C\textsc{ii}}-\text{O}\textsc{i}}(k, \mu)\} &= \{P_{\text{C\textsc{ii}}-\text{O}\textsc{i}}^2(\mu, k) \\
&\quad + (P_{\text{O\textsc{i}}} + P_{\text{N\textsc{ii}}} + P_{\text{C\textsc{ii}}} + P_{\text{O\textsc{i}}}) \times (P_{\text{O\textsc{i}}} + P_{\text{N\textsc{ii}}} + P_{\text{C\textsc{ii}}} + P_{\text{O\textsc{i}}}),
\end{split}
\end{equation}

where \mathcal{P}_{\text{O\textsc{i}}}(k, \mu) is the total [O\textsc{i}] signal auto spectrum, including the interlopers for this line. For simplicity, we approximate the interloper power contamination to the [O\textsc{i}] line as identical to that of the [C\textsc{ii}] line. This should be a good but imperfect approximation, since the two lines lie at fairly similar observed frequencies. Likewise, we approximate the noise power spectrum as identical at the observing frequencies centered around each of the [C\textsc{ii}] and [O\textsc{i}] lines. Based on the local relation between line luminosity and star formation rate in Visbal & Loeb (2010) and using Equation (14), we infer that \langle l_{\text{O}\textsc{i}} \rangle (z = 7) = 0.05 \langle l_{\text{C\textsc{ii}}} \rangle (z = 7). We can then estimate the total signal to noise at which the single parameter, A, may be detected using Equations (27) and (28). For our fiducial numbers, we find that the cross spectrum may be detected at 8.6 - \sigma significance, and so considering the cross spectrum between the two lines seems promising. If the frequency range can be extended somewhat, the cross spectrum between [C\textsc{ii}] and [N\textsc{ii}] might be detectable. In fact, based on the local line-luminosity star formation rate correlation tabulated in Visbal & Loeb (2010), we expect this correlation to be more detectable than that between [C\textsc{ii}] and [O\textsc{i}]: using the numbers in Visbal & Loeb (2010) gives a 17 - \sigma detection forecast. However, assuming that the local relation is especially suspect for [N\textsc{ii}], there is unlikely to be enough prior star formation to build up a significant nitrogen abundance at the high redshifts of interest here (Suginohara et al. 1999).

Unfortunately—for our fiducial survey numbers—we do not expect significant detections of the auto spectra in [O\textsc{i}] or [N\textsc{ii}] given the large interloper “noise” and the lower expected specific intensity in these lines. Consequently, a measurement of the cross spectrum between [C\textsc{ii}] and [O\textsc{i}] and/or [N\textsc{ii}] can help establish the high-redshift origin of a possible [C\textsc{ii}] signal, but it will not provide a full check on the values of \langle l_{\text{O}} \rangle, \langle b_{\text{O}} \rangle inferred from the [C\textsc{ii}] auto spectrum, since the bias and intensity of the [O\textsc{i}] and/or [N\textsc{ii}] emission will remain uncertain.

7. CONCLUSIONS

Line confusion provides an important systematic concern for many IM surveys and for some traditional surveys targeting emission-line galaxies. Interloper line emission will likely be especially strong in future IM surveys aimed at detecting reionization-era signals in the [C\textsc{ii}] and Ly\alpha lines. Here, we developed an approach to fit-out interloper contamination at the power spectrum level, using the fact that the interloper contribution to the emission power spectrum will have a distinctive anisotropy that results when the target redshift is assumed in mapping from frequency and angle to co-moving units.

We applied this to the case of a z = 7 [C\textsc{ii}] IM experiment, in which the z \sim 7 signal fluctuations are expected to be smaller than the combined emission fluctuations from several CO interloper lines. In the limit of low-noise power, the interloper fluctuations can be separated from the [C\textsc{ii}] power spectrum signal. A more sensitive instrument than currently planned is however required. In the near term, it would be interesting to investigate whether the power spectrum anisotropy technique advocated here may be fruitfully combined with a masking approach. Additional careful work is required to study this; in this context, it is crucial to examine optical and infrared tracers to quantify whether they may serve as faithful proxies for the CO interloper emission. We therefore defer this to future work.

We also explored how the IM data cube may be cross-correlated with large-scale structure tracers to extract the properties of likely interloper lines. We showed that emission-line galaxy samples from DESI will be a good data set for cross-correlations, allowing one to extract CO interloper properties for z \sim 7 [C\textsc{ii}] emission surveys. Finally, we briefly considered the cross-correlation between two different fine structure lines at the same redshift; this can help verify the high-redshift origin if a possible signal is seen in the z \sim 7 [C\textsc{ii}] auto spectrum. For all of these studies, it will be important to further consider foreground contamination systematics. Specifically, additional work is needed to quantify the impact of mode-mixing on efforts to measure the angular dependence of the [C\textsc{ii}] power spectrum. It will also be important to quantify how correlated the foregrounds for different tracer lines—such as [C\textsc{ii}] and [O\textsc{i}];—are.

In any case, IM is a potentially powerful approach for tracing large-scale structure at early times and may capture the collective impact of sources that are undetectable using traditional means. Although interloper contamination is a concern for many of these measurements, it may be
circumvented using a combination of techniques, including the power spectrum anisotropy approach considered here.

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