Grounds for Suspicition: Physics-Based Early Warnings for Stealthy Attacks on Industrial Control Systems

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Abstract—Stealthy attacks on Industrial Control Systems can cause significant damage while evading detection. In this article, instead of focusing on the detection of stealthy attacks, we aim to provide early warnings to operators, in order to avoid physical damage and preserve in advance data that may serve as an evidence during an investigation. We propose a framework to provide grounds for suspicion, i.e., preliminary indicators reflecting the likelihood of success of a stealthy attack. We propose two grounds for suspicion based on the behaviour of the physical process: (i) feasibility of a stealthy attack, and (ii) proximity to unsafe operating regions. We propose a metric to measure grounds for suspicion in real-time and provide soundness principles to ensure that such a metric is consistent with the ground for suspicion. We apply our framework to Linear Time-Invariant (LTI) systems and formulate the suspicion metric computation as a real-time reachability problem. We validate our framework on a case study involving the benchmark Tennessee-Eastman process. We show through numerical simulation that we can provide early warnings well before a potential stealthy attack can cause damage, while incurring minimal load on the network. Finally, we apply our framework on a use case to illustrate its usefulness in supporting early evidence collection.

Index Terms—Cyber-physical systems, industrial control systems, early warning systems, security, process control, reachability analysis

1 INTRODUCTION

Cyber-physical Systems (CPS) augment physical systems with enhanced capabilities, such as real-time monitoring and dynamic control [1]. Industrial Control Systems (ICS) are considered a subclass of CPS, where software controls safety-critical industrial processes. Attacks against ICS can have disruptive consequences to users and physical assets, as shown by the German steel mill attack in 2014 [2] and the attack against the Ukrainian power grid in 2015 [3] — among others.

Anomaly-based Intrusion Detection Systems (IDS) can usually detect attacks affecting the physical process in an ICS, by monitoring deviations from the normal system behaviour (anomalies) [4]. However, skilled attackers can take advantage of the noise in the system and the thresholds used by the anomaly detectors, to cause damage to the ICS before an alarm is raised [5], [6]. Such attacks which evade detection are also known as stealthy attacks. Early Warning Systems (EWS) [7], [8] traditionally monitor the occurrence of suspicious and seemingly benign network events (often called weak evidence). Differently from IDS, EWS generate predictions and advice on unfamiliar situations before a potential attack can cause harm [8]. EWS may not reveal attacks on their own, but can guide the selection of appropriate measures to detect potential intrusions, and as such complement existing IDS as a security solution [9]. In this paper, instead of forcing the detection of stealthy attacks, we aim to raise early warnings when there is sufficient evidence that a potential stealthy attack can cause damage.

Our main contribution is a framework to generate early warnings in ICS based on preliminary indicators of a stealthy attack, referred to as grounds for suspicion. This framework can be used within a larger EWS which considers indicators from other sources. The success of a stealthy attack depends on the laws of physics underlying the behaviour of the ICS and the anomaly detector. Thus, we define two grounds for suspicion based on the physical state of the system: (i) Feasibility of a stealthy attack indicates whether the ICS can be taken to an unsafe operating region, while avoiding detection by the IDS. (ii) Proximity represents the vicinity of the system to the unsafe operating region. To monitor the grounds for suspicion, we propose a suspicion metric based on a mathematical model of the system and a notion of reachability. We also provide soundness principles to ensure that a metric is consistent with the measured grounds for suspicion.

To assess feasibility of our framework, we study its applicability to Linear Time-Invariant (LTI) systems, a standard physical modelling framework commonly used in process control. We adapt existing reachability analysis...
tools [10] to compute the suspicion metric. We alleviate the computational cost of performing real-time reachability analysis by computing symbolic reachable sets of system states offline [11]. We then instantiate these sets online given a prediction of the physical state variables for a certain number of time steps into the future. We leverage ellipsoidal techniques [12], [13], [14] to perform efficient safety checks online and compute the suspicion metric. In a previous work [15], we focused on performing safety checking for LTI systems under stealthy attacks in real-time. In the present work, we extend these results into an algorithm that efficiently computes the suspicion metric online. We also design suitable thresholds for warnings of different criticality and show how our algorithm satisfies the soundness principles of our framework.

We validate our framework’s application to LTI systems using a testbed involving a networked version of the benchmark Tennessee-Eastman Process (TEP). We use numerical simulations to showcase that our framework can generate early warnings before a stealthy attack can cause damage. Although we perform this study using a particular type of stealthy attack — false data injection on sensors — our framework is generalizable to other types of stealthy attacks. Furthermore, we demonstrate that our framework scales well with the number of safety constraints and incurs minimal load on the network. Finally, we apply our framework on a use case inspired by the TEP benchmark, to showcase its usefulness in supporting early evidence collection, especially from low-level control devices. However, these benefits come with a cost associated with the human effort required to instantiate the framework.

The rest of the paper is organised as follows. Section 2 provides a brief overview of related work. Section 3 illustrates a motivating example, while Section 4 describes the main contribution of the paper, which is the framework for physics-based early warnings. We begin our case study in Section 5 where we introduce the TEP benchmark. In Section 6 we explain how we instantiated our framework to the benchmark. Section 7 presents our evaluation results, and Section 8 concludes the paper.

2 RELATED WORK

In this section, we provide some background on existing attack detection techniques in ICS. We also clarify the positioning of the paper with respect to existing work on early warning systems and attack impact assessment in CPS/ICS.

2.1 Attack Detection in ICS

Several network-based intrusion detection systems for CPS, and particularly for ICS, have been suggested in previous work. Some of them [16], [17] are knowledge-based and look for features in the network traffic that are consistent with a known threat model. Others [18], [19] are anomaly-based and look for features that suggest a deviation from the expected behaviour. Furthermore, physics-based methods [4] consider the effect of attacks on the controlled physical process, and look for deviations from expected physical sensor measurements, given by a mathematical model of the system.

However, with enough knowledge about the system, an offender can launch stealthy attacks. These attacks are usually performed by introducing fake sensor measurements or actuation signals in the control loop. In this way, the anomaly detector will not be able to detect a deviation of the system from the normal behaviour. Stealthiness of such attacks can be ensured by mimicking the noise native to the system [5] or exploiting some control-theoretic properties [6], [20] (e.g., zero dynamics). “Active” detection methods have been proposed to detect stealthy attacks. These methods involve the introduction of a probing signal (watermark) to reveal fake sensor measurement or actuation signals [21], [22]. Active methods can also be designed for attacks exploiting specific control-theoretic properties. In this case, detection relies on modifying the system by, for example, including additional sensor measurements [20] or modulating actuation signals [23]. These modifications can remove the control-theoretic properties exploited by the attack.

However, active attack detection techniques may bring trade-offs that can jeopardise their effectiveness. In the case of physical watermarking, the trade-off between the watermark’s robustness and the control performance may not be acceptable, especially in safety-critical systems. Also, modifying the structure of the system (e.g., by adding sensor measurements) is often hard and expensive.

2.2 Early Warning Systems

EWS combine preventive measures, such as risk and vulnerability assessment, with IDS, to provide a clearer “picture” of the security situation and send warnings about potential network intrusions [7]. They are regarded as a complementary solution to existing IDS/ADS, where their main benefit lies in providing predictions of potential harm in unfamiliar situations, typically with zero-day attacks [9].

Traditionally, IDS/ADS exist as a reactive security solution where alarms are generally based on either a clear deviation from normality or a strong evidence of misuse. Differently from these systems, EWS proactively collect, accumulate, and combine events that don’t necessarily form part of a known attack signature or a clear anomaly in order to form a better picture of the security situation. For example, Chivers et al. [24] consider events such as failed connections, failed logins, and anomalous phone calls to be weak indicators of malicious insider activity. Such events by themselves may not be considered by an IDS/ADS. These indicators are then aggregated and accumulated using a Bayesian score that reflects the probability of a node being subverted. Furthermore, EWS go beyond IDS/ADS by incorporating a mechanism to predict potential harm to the system using, for instance, statistical modelling as in the work of Abbaszadeh et al. [25]. While EWS by themselves may not necessarily detect attacks, they can guide the selection of actions that may in turn reveal a potential intrusion. For example, the framework proposed by Brignoli et al. [26] allows the evaluation of the potential impact of active countermeasures in IoT networks.

Recently, a growing body of work has considered this approach in traditional IT systems to tackle slow and stealthy attacks [9]. Apel et al. [27] proposed an EWS that relies on intelligence sharing between different organisations to counter advanced coordinated attacks at their early stages.
Kalutarage et al. [28], [29] proposed a Bayesian approach, which accumulates evidence over long periods of time to counter network attacks in their reconnaissance phase. The reader is referred to the work by Ramaki et al. [9] for a comprehensive survey of existing work on EWS and a more detailed comparison of EWS and IDS/ADS.

To the best of our knowledge, a very limited number of works apply EWS to ICS. One exception is the recent work by Abbaszadeh et al. [25], which generates early warnings based on potential anomalies predicted by learning time series behaviour. Instead of relying on training statistical models, we use in our work ideas from reachability analysis based on a standard identified model of the system.

Other related work in the context of ICS/CPS has proposed online monitoring techniques based on a notion of proximity to a predefined set of unsafe or critical states [30], [31], [32], [33]. For example, Carcano and Coletta [31], [32] proposed the use of distance metrics such as euclidean distance to a set of unsafe states represented as boolean expressions over state variables. Castellanos and Zhou [33] further extended this notion by computing an approximate “time-to-critical” states metric, based on euclidean distance and the rate of change of the physical states. Similarly to these approaches, we compute proximity from the current state of the system which is estimated based on received sensor values. However, this estimated state may not be representative of the state of the system if the latter is under a stealthy attack. Thus, our notion of proximity bounds — with a certain confidence level — the actual state of the system. To generate early warnings before a stealthy attack can cause damage, we also predict the state of the system for a certain number of time steps in the future. This prediction is similar to the work by Etigowni et al. [30] and relies on an approximated model of the system and the monitoring of controller states.

Bradford et al. [34] proposed the idea of a tiered approach for EWS. First, they profile agents in a system by accumulating preliminary data, then they perform more detailed investigations and intensive data collection if some predefined thresholds are crossed. Chivers et al. [24] implemented a layered approach for insider attacks in networked systems, while Kalutarage et al. [35] did it for cyber conflict attribution. Differently from this work, we focus on generating early warnings about stealthy attacks in ICS. The novelty of our approach lies on the measurement of grounds for suspicion based on the physical state of the ICS.

2.3 Attack Impact Assessment in CPS/ICS

Our work builds on recent research assessing the physical impact of stealthy attacks on CPS and ICS. In particular, we adapt techniques based on reachability analysis [10], [36], [37] to provide measures of the proposed grounds for suspicion. While in previous work such techniques were mainly employed to assess the security of a system and perform offline risk analysis, here we adapt them for online monitoring.

Existing risk assessment approaches in the context of ICS security are based on the assumption that the system will have steady states when subjected to an attack. However, this assumption can fail when long transients are experienced in operating conditions. This is true in the process industry, where changes in operating conditions are frequent due to external disturbances and real-time optimisation requirements [38].

In our instantiation of the framework to LTI systems, our approach is similar to that of Kwon et al. [37]. However, the main difference is that Kwon’s algorithm is designed specifically to cater for Unmanned Aerial Vehicles (UAV) applications, where safety constraints are time-varying and have a different mathematical expression to constraints typically found in process control applications that we consider. Furthermore, Kwon’s algorithm requires updating the reachable ellipsoid at each time step through a recursive structure, which may be resource-intensive as it is not clear it can scale well with a large number of state variables typically found in process control applications.

Finally, several approaches exist to assess the impact of stealthy attack strategies in CPS/ICS. For example, on the one hand, Milosevic et al. [39] propose the use of the infinity norm of critical states after a certain time period and present a framework for security measure allocation offline given attack complexity and impact measures. Urbina et al. [40], on the other hand, consider the rate of change of the physical variables under a stealthy attack as a measure of impact. In this paper, we do not focus our attention on computing the impact of a stealthy attack. Instead, we generate early warnings in real-time depending on the likelihood of a stealthy attack to be successful.

3 Motivating Example

Consider a chemical reactor equipped with a controller that keeps the level of liquids in the reactor at a desired set-point (Fig. 1). An attacker with access to channels communicating level values to the controller, wishes to cause physical damage to the system. To maximise chances of success and avoid detection, the attacker uses his/her knowledge of the physical behaviour of the system (obtained through reconnaissance activity) and its anomaly detector.

The attacker takes advantage of the safety-critical operating mode of the reactor, and modifies level sensor values such that the bias between real and received values grows slowly over time. This in turn tricks the controller into slowly increasing the level in the reactor, which is driven to the point of overflow (top part of Fig. 2). This may have significant consequences, such as a fire, especially if the reactor is operating at high temperature or pressure. In addition, data stored on low-level control devices (e.g., Programmable Logic Controllers’ (PLC) configurations, sensor/actuator
4.1 Framework Structure

Fig. 3 shows an instantiation of our framework to a control system. The latter mainly takes as input estimates of physical state variables provided by some state estimator as well as the current state of the controller(s). These estimates are then used to measure the feasibility and proximity grounds for suspicion, which act as weak evidence of a stealthy attack by reflecting its likelihood of success. These two grounds are then combined and measured via a suspicion metric, which in turn reflects their evidentiary weight, and triggers a warning when crossing a certain threshold. Depending on the criticality of the crossed threshold, different actions may follow, such as further evidence collection or safety measures initiation. Identification of these actions is outside the scope of this work.

4.1.1 Grounds for Suspicion

An attacker wishing to avoid detection will manipulate the system in a way that keeps the difference between estimated predictions and actual sensor readings sufficiently small. Our framework does not attempt to distinguish an anomalous behavior by comparing the two. Instead, it measures the following grounds for suspicion:

- **Feasibility of a Stealthy Attack**: given the dynamics of the system and the constraints imposed by the anomaly detector, we check whether the current state of the system can be taken to an unsafe state (hence causing damage) while avoiding any alarm in the process.
Proximity to Unsafe States: given the current state of the system, if an attack is actually taking place without having been detected, we monitor how far would the system be from reaching an unsafe operating region. The closer the system is to this region, the more likely a stealthy attack is successful, as the attack may take less time to achieve its goal.

The feasibility of a stealthy attack and the proximity of the system to an unsafe state do not necessarily imply that a malicious activity is taking place. However, they can indicate that a stealthy attack may successfully damage the system. Hence, we consider them to be weak evidence of a potential stealthy attack, in the same manner a failed login attempt may be suspicious but cannot be used as evidence of an intrusion.

4.1.2 Suspicion Metric

The evidentiary weight of events that can trigger early warnings is typically measured using a certain metric. For example, Chivers et al. [24] assign a Bayesian score to network nodes that generate events considered as weak evidence. We propose an analogous score, called suspicion metric. This metric essentially measures in real-time the likelihood that a potential stealthy attack will cause damage to the system before being detected by combining these two grounds for suspicion. At runtime, a human operator would be provided with the evolution of the suspicion metric over time (Fig. 3). If the metric crosses a certain threshold, a warning is raised.

4.2 Suspicion Metric Soundness Principles

As several types of physical systems can be modelled with different formalisms (e.g., continuous-state versus discrete-event/hybrid), we do not attempt to propose a formula to compute a suspicion metric. Instead, we provide soundness principles, so that irrespective of the system where the framework is instantiated, the metric can reflect the grounds for suspicion in a sound manner:

1) The metric must include at least one clear threshold which if crossed, a warning is issued. We propose two thresholds (Fig. 3): (i) one of low-criticality, which may trigger intensive data collection to proactively check for intrusions; and another (ii) of high-criticality typically triggering measures preventing a safety incident.

2) The metric should increase over a certain time interval if a) the likelihood of the real physical state of the system diverging from the provided estimate and evolving into an unsafe operating region is increasing (feasibility); or b) if the system is evolving closer to unsafe states meaning that a potential attack is less and less time consuming for the attacker (proximity).

The first principle ensures that the EWS can advise an operator about the current security situation. The second ensures that the metric provides a measures the evidentiary weight of the grounds for suspicion and can inform operators about the likelihood of success of a potential stealthy attack.

4.3 Framework Configuration Requirements

The configuration of the framework involves mainly providing measures of feasibility and proximity to construct a suspicion metric according to the soundness principles provided earlier. This can be performed by reusing existing techniques proposed in the domain CPS/ICS security. For example, techniques to compute reachable sets under a given stealthy attack [10], [37] can be used to measure feasibility, while distance metrics such as the euclidean or Hamming distance, can be used to measure proximity given the real-valued nature of most physical state variables.

Therefore, to configure the framework, we require mainly (i) a mathematical model of the system, including its controller and the unsafe operating region; (ii) information on the used anomaly detection method; and (iii) a model of an attack at the level of physical process. Note that (i) is standard in control engineering and safety analysis, while the threat model (iii) is only required to show the effect of a potential attack on the control loop. There exist several works [44], [45] that provide effective ways of modelling such effects.

In this paper we focus on applying the framework to systems that can be modelled using the Linear-Time Invariant (LTI) modelling framework — we defer the study of other systems to future work. Given a certain operating range, several control systems can be approximated with high accuracy by an LTI model using well-established techniques. This
5.1 Physical System and Controller

The evolution of the physical state of a standard, frequently used Linear-Time Invariant (LTI) model is given as follows:

\[
\begin{align*}
    x(k+1) &= Ax(k) + Bu(k) + w(k) \\
    y(k) &= Cx(k) + v(k)
\end{align*}
\]  

(1)

The matrices \( A, B, \) and \( C \) are real, time-invariant, and of appropriate dimensions. The state of the system is given by the vector \( x(k) \in \mathbb{R}^n \), sensor measurements by \( y(k) \in \mathbb{R}^m \) and control input by \( u(k) \in \mathbb{R}^p \) where \( k = t / \Delta t \in \mathbb{N} \) denotes discrete time instants with \( \Delta t \) being the sampling period. Process disturbances \( w(k) \) and sensor noise \( v(k) \) are assumed to follow a zero-mean Gaussian distribution with covariance matrices \( \Sigma_1 \) and \( \Sigma_2 \), respectively. We assume that the system is observable and controllable in a control-theoretical sense. Furthermore, the system is equipped with an output feedback control loop, such that given received sensor measurements \( \hat{y}(k) \) and a set-point reference \( y_r(k) \), a control signal \( u(k) = K[y_r(k) - \hat{y}(k)] \) based on the control law \( K[\cdot] \) is sent to the process at each time step. We assume that the system is stabilised by this controller.

A subset of state variables, denoted as “critical”, and grouped in a vector \( x_c = \{x_c \} \), \( x_c \in \mathbb{R}^n_c \), \( C_c \in \mathbb{R}^{n_c \times n} \), are required to remain within certain bounds to ensure safe operation. Unsafe conditions can be written in the form of a linear combination of the state variables. Thus each linear combination of state variables denoting safety constraints can be geometrically interpreted as a half-space in \( \mathbb{R}^n \). Let \( S_u \) denote the unsafe operating region, this can in turn be interpreted as a union of half-spaces as follows:

\[
S_u = \{ x(k) \in \mathbb{R}^n \mid \bigcup_{i=0}^{n_c} C_{c,i} x(k) \geq b_i \}.
\]  

(2)

Where \( b_i \) denotes the safety bound on the \( i^{th} \) critical state variable (or the \( i^{th} \) half-space scalar from a geometric point of view), and \( C_{c,i} \) denotes the \( i^{th} \) row of the matrix \( C_c \).

Although our main concern in this paper is with stealthy attacks that seek to cause physical damage to the system, our modelling framework can accommodate other objectives for stealthy attacks. For example, if we are worried about attackers causing economic loss by driving the system to an “expensive” operating state, then the relevant state variables and constraints can be added to \( S_u \) to express such an expensive operating region. We are planning to consider this type of stealthy attacks in future work.

5.2 Anomaly Detector

At a time \( k_0 \), given previous estimates and control actions, the state estimate \( \hat{x}(k) \) and expected sensor measurements \( \hat{y}(k) \) are provided by a Kalman filter.
\[
\begin{aligned}
\dot{x}(k) &= A\hat{x}(k-1) + Bu(k-1) \\
&
+ L(\hat{y}(k-1) - C\hat{x}(k-1)). \\
\hat{y}(k) &= C\hat{x}(k)
\end{aligned}
\]

Where the design parameter \(L\) is the observer gain matrix, the existence of which is guaranteed by the observability of the system. The estimated sensor measurement \(\hat{y}(k)\) is compared with the received value \(y(k)\) using a residual metric; \(r(k) := y(k) - \hat{y}(k)\). Under nominal conditions, the residual metric has a zero-mean and a covariance matrix \(\Sigma\). To check for this hypothesis, a chi-squared metric, \(z(k) = r(k)^T \Sigma^{-1} r(k)\) is computed and compared with a threshold \(\tau\), such that exceeding this threshold implies a possible anomaly and raises an alarm. \(\tau\) can be set according to a desired false alarm rate \(\beta\). The reader is referred to [47] for more detail on the derivation of the observer gain matrix \(L\), the anomaly detection threshold \(\tau\), and the residual’s covariance matrix \(\Sigma\) under nominal conditions.

### 5.3 Threat Model

In this paper we consider false data injection attacks on sensors, which consist of falsifying sensor values such that the controller drives the system into unsafe operating levels. Such attacks are typically modelled as a bias imposed on \(y(k)\) [45]. Let \(\{k_s, \ldots, k_f\}\) be the time period of the attack, the actual sensor readings \(\hat{y}(k)\) received by the controller are then given as

\[
\hat{y}(k) = \begin{cases} 
    y(k) + \delta(k) & \forall k \in \{k_s, \ldots, k_f\}; \\
    y(k) & \text{otherwise}
\end{cases}
\]  

Under such attack, the anomaly detector’s chi-squared metric is given by

\[
z(k) = (y(k) - \hat{y}(k) + \delta(k))^T \Sigma^{-1} (y(k) - \hat{y}(k) + \delta(k)).
\]

The attacker, having knowledge of the anomaly detector parameters (i.e., \(\Sigma, \beta\) and \(\tau\)) can maintain the stealthiness of the attack by ensuring that \(\delta(k)\) maintains a nominal false alarm rate; i.e., \(\Pr[z(k) \leq \tau] = 1 - \beta\). We use this characterisation of a stealthy attack because it represents more realistically an advanced attacker wishing to remain stealthy until at least achieving the objective of damaging the system. In practice, given \(K\) time steps, the attacker may choose to raise alarms for \(\beta K\) steps; thus mimicking the false alarm rate as closely as possible. Due to space limitations, the reader is referred to [47] for a more detailed description and analysis of the distribution of the detector metric under such attack.

### 6 Instantiating the Proposed Framework for LTI Systems

The proposed physics-based EWS component takes as input the vector of estimated state variables \(\hat{x}\) in addition to the state of the controller. We initialise the suspicion metric \(\text{SUSP}\) as a function of two terms: feasibility \(\text{FEAS}\) and proximity \(\text{PROX}\). In this section, we instantiate the proposed framework for the system described in Section 4. We use analysis tools from the literature to construct a formula for \(\text{FEAS}\) and \(\text{PROX}\). In a previous work [15], we showed how to perform efficient online safety checking for LTI systems under stealthy attacks. In this section, we describe the safety checking algorithm and we extend it by including the suspicion metric. We also design thresholds for warnings of different criticality to apply the algorithm to the proposed framework. We also show how the proposed algorithm satisfies the soundness principles proposed in Section 4.

#### 6.1 Feasibility Measure

The attack in (4) is defined to be feasible if (i) the corrupting signal can maintain the nominal false alarm rate throughout the attack and (ii) at the end of the attack the system can be driven to unsafe operation. This can be stated as a reachability problem. Namely, let \(R_x(k)\) be the set of reachable states at time \(k\) due to the attack (4)

\[
R_x(k) = \{x(k) \in \mathbb{R}^n \mid x(k) \text{ is s.t. (1)} \land \delta(k) \text{ is s.t. } \Pr[z(k) \leq \tau] = 1 - \beta\}.
\]

The attack (4) is then feasible at time \(k\) if, for the next \(K\) time instants, there exists an instant \(k_f \in \{k, \ldots, k + K\}\) such that \(R_x(k_f) \cap S_u \neq \emptyset\). As a measure of feasibility, we propose to use a function of the size of this intersection. However, computing \(R_x(k)\) and the size of \(R_x(k_f) \cap S_u\) exactly in real-time is intractable. Furthermore, since \(x(k)\) is partially driven by the Gaussian noise \(w(k)\) which has an infinite support, computing \(R_x\) using deterministic methods will yield an unbounded set.

We address intractability by approximating a symbolic reachable set offline parametrised by the state estimate. We compute the resulting set under the assumption of a bound on the energy of the noise with a certain confidence level, thus preventing unbounded reachable sets. As such, computing the feasibility measure (and subsequently the suspicion metric) involves an offline initialisation step as well as online emptiness checks of \(R_x(k_f) \cap S_u\).

#### 6.1.1 Offline Initialisation

To approximate a symbolic reachable set offline parameterised by the current state estimate, we consider the reachable set \(R_e\) of the estimation error \(e(k) := x(k) - \hat{x}(k)\) under an attack. Assuming the initial error at the beginning of an attack is always almost zero, this set is independent of the physical state at the start of the attack. Hence, computing it offline would provide a symbolic reachable set as a function of the provided state estimate, which can then be instantiated online. We use the method proposed by Murgaia et al. [10] to compute an ellipsoidal approximation of the reachable set of estimation error under a stealthy attack.

Based on Equation (3), the estimation error under an attack evolves according to the following:

\[
e(k + 1) = Ae(k) - L(y(k) - \hat{y}(k) + \delta(k)) + w(k).
\]  

To address the problem of computing \(R_e\), when the error is partially driven by the Gaussian noise \(w(k)\) and the attack-dependent sequence \(\delta(k) = y(k) - \hat{y}(k) + \delta(k)\), we set a confidence level on the energy of both of these vectors. Given the threat model described in (4), we have for the sequence \(\delta(k)\) that \(\Pr[z(k) \leq \tau] = \Pr[\|\Sigma^{-1/2} \delta(k)\|^2 \leq \tau] = 1 - \beta\) where \(\|\cdot\|\) denotes the \(L_2\)-norm. As for the noise, since it follows a
Gaussian distribution, a bound $\bar{w}$ on its energy $\|w(k)\|^2$ can be set for a desired confidence level $p = \Pr[\|w(k)\|^2 \leq \bar{w}]$ using the gamma or the chi-squared distribution [10], [47].

Using this truncation of the distribution of $\delta(k)$ and $w(k)$, we compute an ellipsoidal approximation $\mathcal{E}_p$ of $\mathcal{R}_p$ offline for a desired confidence level $p$. A larger confidence level would lead to a larger set, at the cost of being overly conservative with the emptiness checks. A reasonable choice for $p$ would be $1 - \beta$, as the false alarm $\beta$ is designed to be small. This also simplifies the computation of the reachable set, since for $p = 1 - \beta$, we readily have $\Pr[\|w(k)\|^2 \leq \bar{w}] = \Pr[z(x) \leq \tau]$ under the attack in (4).

Given the system model (1), the Kalman gain $L$, the anomaly detector threshold $\tau$, and the $p$-probable bound $\bar{w}$ on the process noise energy, it is possible to compute an ellipsoidal approximation $\mathcal{E}_p \supseteq \mathcal{R}_p$ of the following form:

$$\mathcal{R}_p \subseteq \mathcal{E}_p = \{e(k) | e^T(k)\mathbf{II}^{-1}e(k) \leq 1\}. \tag{8}$$

Where $\mathbf{II}$ is called the ellipsoid’s shape matrix. The computation of $\mathbf{II}$ involves solving a Linear Matrix Inequality (LMI) problem given the aforementioned parameters. Note that since we assume the system to be stable, the matrix $\mathbf{II}$ exists [10]. Due to space limitations, the reader is referred to [10] and [47] for more details on this procedure and the effect of the choice of $p$ on the tightness of the ellipsoidal approximation.

Note that this step is performed only once offline, and only the matrix $\mathbf{II}$ needs to be stored for online emptiness checks. Therefore, the computation of this ellipsoidal approximation does not affect real-time performance. Given the matrix $\mathbf{II}$, and replacing $e(k)$ by its definition, we obtain a symbolic ellipsoidal approximation $\mathcal{E}_p^s(\hat{x}(k))$ of the reachable set $\mathcal{R}_p^s(x(k))$ of the actual system state $x(k)$, parameterised by the current state estimate $\hat{x}(k)$

$$\mathcal{R}_p^s(x(k)) \subseteq \mathcal{E}_p^s(\hat{x}(k)) = \{x(k) \in \mathbb{R}^n | (x(k) - \hat{x}(k))^T\mathbf{II}^{-1}(x(k) - \hat{x}(k)) \leq 1\}. \tag{9}$$

This ellipsoidal approximation can then be instantiated online at a time $k$ given the current state estimate $\hat{x}(k)$.

### 6.1.2 Online Emptiness Checks

At runtime, given the current physical state estimate and the state of the controller, we predict the state of the system for $K$ steps into the future using the identified model of the system. For each predicted state $\hat{x}(k+l)$, $l \in \{0, \ldots, K\}$, we instantiate the ellipsoidal approximation $\mathcal{E}_p^s(\hat{x}(k+l))$ of the reachable set under a potential stealthy attack. Since the reachable ellipsoids computed offline are parametrised by the state estimate (Equation (9)), we can instantiate them at each predicted state without the need for further operations. Upon encountering a state where $\mathcal{E}_p^s(\hat{x}(k+l)) \cap \mathcal{S}_u \neq \emptyset$, the prediction stops, and we compute the size of this intersection as a feasibility measure.

At each predicted state $\hat{x}(k+l)$, we take advantage of the ellipsoidal nature of $\mathcal{E}_p^s(\hat{x}(k+l))$ and the fact that $\mathcal{S}_u$ can be interpreted geometrically as a union of half-spaces to perform efficient emptiness checks of their intersection. For each hyperplane delimiting a half-space in $\mathcal{S}_u$, we compute the distance from the ellipsoid $\mathcal{E}_p^s(\hat{x}(k+l))$. The intersection is then non-empty if the distance value is negative [12].

When the intersection is non-empty, it is possible to approximate the intersection of $\mathcal{E}_p^s(\hat{x}(k+l))$ with each of the half-spaces $\mathcal{H}_i \subseteq \mathcal{S}_u$ using an ellipsoid $\mathcal{E}_p^i$ of shape matrix $\mathbf{II}_i$. Boyd and Vandenberghe [14] provide an equation to efficiently compute this shape matrix, which we omit here for brevity. We use the ratio of the volume of this approximate ellipsoid to the reachable ellipsoid to measure feasibility

$$\text{FEAS}(k) = \frac{V_{\mathcal{E}_p^i}}{V_{\mathcal{E}_p}}. \tag{10}$$

Where $V_{\mathcal{E}_p^i} = \max_{i=1,\ldots,n} \{\text{vol}(\mathcal{E}_p^i)\}$ is the maximum intersection volume obtained at time $k+l$ among the intersections of $\mathcal{E}_p^s(\hat{x}(k+l))$ with each of the half-spaces $\mathcal{H}_i \subseteq \mathcal{S}_u$. $V_{\mathcal{E}_p} = \text{vol}(\mathcal{E}_p)$ is the volume of the reachable ellipsoid.

### 6.2 Proximity to Unsafe States

Given the real-valued nature of the physical state variables, one can employ a simple measure based on euclidean distance to compute the proximity of the system to the set of unsafe states. This approach was employed by Coletta et al. [32]. However, as the actual state of the system may be different from the given estimate (due to a potential stealthy attack), this simple distance measure may not reflect the actual proximity of the system to unsafe operating region. Such measure also does not reflect how fast the system may evolve to an unsafe state under a potential stealthy attack.

We make use of the procedure used to compute the symbolic reachable set explained in Section 6.1.2. If we find that $\mathcal{E}_p^s(\hat{x}(k+l)) \cap \mathcal{S}_u \neq \emptyset$ for an $l = \tilde{l}$, then we can conclude that under a potential stealthy attack, the system may be damaged after at least $l$ time instants. Hence, we use the following as a measure of proximity

$$\text{PROX}(k) = 1/(1 + \tilde{l}). \tag{11}$$

### 6.3 Algorithm and Metric Soundness

Algorithm 1 outlines the steps taken online to perform online safety checks and compute the suspicion metric. The computation of this metric consists of three main steps: (1) Given the current estimated state $\hat{x}(k)$ of the system and the state of controllers, we predict the evolution of the state for a specified number of time steps into the future. Note here that there is no need for an assumption on the value of a potential attack $\delta(k)$, as the reachable set instantiated at the predicted states will contain the real state of the system if it is indeed under an attack. (2) For each predicted state, the approximate reachable set under stealthy attacks is instantiated and emptiness checks of its intersection with the set of unsafe states are performed. (3) If the intersection is non-empty at a time $k+l$, the prediction stops, and the suspicion metric is computed as follows:

$$\text{SUSP}(k) = \text{FEAS} \times \text{PROX} = \frac{V_{\mathcal{E}_p^i}}{V_{\mathcal{E}_p}(1 + \tilde{l})}. \tag{12}$$

If the intersection is empty for all the states predicted within the specified number of steps, then $\text{SUSP}(k) = 0$. 
Algorithm 1. Computing the Suspicion Metric Online

\begin{align*}
\text{Inputs:} & \quad (K, \mathbf{I}, \hat{x}(k), \text{ControlState}, \mathcal{S}_u) \\
1: & \quad \hat{x}_p \leftarrow \hat{x}(k) \\
2: & \quad \text{for all } l \in \{0, \ldots, K\} \text{ do} \\
3: & \quad \text{ReachEll} \leftarrow \text{ELLIPSOID}\hat{x}_p, \mathbf{I} \\
4: & \quad \text{for all } \mathcal{H}_{p,i} \subset \mathcal{S}_u \text{ do} \\
5: & \quad \text{DistToUnsafe} \leftarrow \text{DIST ReachEll, Hyperplane} \\
6: & \quad \text{if DistToUnsafe} < 0 \text{ then} \\
7: & \quad \text{Raise non-empty intersection flag and compute the shape of the intersection ellipsoid} \\
8: & \quad \text{isNonEmpty} \leftarrow \text{FALSE} \\
9: & \quad \text{II}_l \leftarrow \text{ELLINTERSECT ReachEll, Hyperplane} \\
10: & \quad V_{E_l} \leftarrow \text{VOLUME II}_l \\
11: & \quad \text{else} \\
12: & \quad V_{E_l} \leftarrow 0 \\
13: & \quad \text{end if} \\
14: & \quad \text{end for} \\
15: & \quad \text{if isEmpty then} \\
16: & \quad \text{Break the loop and return the suspicion metric} \\
17: & \quad \text{FEAS} \leftarrow \text{MAX } V_{E_l} / \text{VOLUME ReachEll} \\
18: & \quad \text{PROX} \leftarrow 1/(1 + l) \\
19: & \quad \text{SUSP} \leftarrow \text{FEAS} \times \text{PROX} \\
20: & \quad \text{return SUSP} \\
21: & \quad \text{end if} \\
22: & \quad \text{end for} \\
23: & \quad \text{Return 0}
\end{align*}

6.3.1 Algorithm Complexity

In Algorithm 1, the prediction of the state of the system relies on an identified LTI model. As evident from Equation (1), the computation of the next state involves mainly vector addition and matrix-vector multiplication — operations that scale polynomially with the number of physical states. Thus, given a fixed number of physical states, the prediction is expected to scale linearly with the maximum number of time steps for prediction \( K \). Furthermore, checking the emptiness of the intersection of the current reachable ellipsoid with the set of unsafe states relies on computing the distance between the two sets. This distance, whose formula can be found in [12], relies also on performing matrix-vector multiplication and computing vector norms, which scales polynomially with the number of states. For a fixed number of states, and since this distance is computed for each safety condition in the set of unsafe states, the emptiness checks will scale linearly with the number of safety constraints. The same reasoning applies to the matrix intersection procedure [14] and its corresponding volume, which involves matrix addition and determinant operations. Several constant parameters involved in the computation of ellipsoid-to-half-space distances, the intersection between the two sets, and the feasibility metric can be pre-computed offline to improve real-time performance. These parameters include the volume of the pre-computed reachable ellipsoid and the norms of the half-space normal vectors \( C_{E_i} \) (Equation (2)) representing safety conditions.

6.3.2 Metric Soundness

An increase in the value of the metric can imply one of the following: (i) \( \bar{V}_{E_t} \) is increasing, indicating that it is becoming increasingly likely for the actual state of the system to diverge from the estimate and enter an unsafe operating region due to a stealthy attack; (ii) \( \bar{l} \) is decreasing, indicating that the system is in increasing proximity to unsafe operation regions. Thus, the proposed metric serves as a measure of likelihood of the attacker being able to take the system into unsafe states (feasibility) penalised by the number of time steps required to damage the system (proximity).

To raise physics-based early warnings, we propose two thresholds based on the value of \( \bar{l} \) returned by Algorithm 1. This value indicates the time that would be needed by a potential attack to cause damage before being detected. Let \( l_1 \) be the time required by the operators to perform necessary preemptive actions after a low-criticality warning, and let \( l_2 \) be the time necessary to perform potentially more drastic actions after a high-criticality warning, with \( l_2 < l_1 \). \( l_1 \) and \( l_2 \) can be set based on expert knowledge of the system in question and the post-warning measures to be taken.

Accordingly, we set two conditions for different criticality thresholds in this case study:

1. A “low-criticality” warning is raised when \( \bar{l} \leq l_1 \) and \( \bar{V}_{E_{t_1}} / \bar{V}_E \geq 0.5 \). These conditions imply that if the system is under a potential stealthy attack, the damage will likely take place after at most \( l_1 \) time instants. However, \( l_1 \) is sufficient to perform preemptive low-criticality actions, such as collecting potential evidence of an attack.

2. A “high-criticality” warning is raised if the suspicion metric shows that the attacker is likely to cause damage in a smaller time frame. Namely, this type of warning can be raised when \( \bar{l} \leq l_1 \) and \( \bar{V}_{E_{t_1}} / \bar{V}_E \geq 0.5 \) with \( l_2 < l_1 \). In this case, high-criticality preemptive actions can be taken, such as engaging safety measures.

The above discussion shows that the proposed metric satisfies the soundness principles proposed in Section 4.

7 Evaluation

In this section, we describe the virtual testbed that we used to evaluate our framework. Using numerical simulations we validate whether our framework can warn well in advance of damage caused by a potential stealthy attack. We also assess scalability and network performance of our framework. Finally, we discuss the usefulness of our framework in supporting early evidence collection in a use case scenario. All activities conducted to support the evaluation were performed on an Intel i7–9750H CPU clocked at 2.6 GHz with 16 GB of RAM memory.

7.1 Virtual Testbed

To evaluate our framework we rely on a modified simulation of the Tennessee-Eastman Process (TEP) [48]. This is a benchmark chemical process which is used extensively to study problems in the process control field [49]. The process involves an exothermic reactor and units to separate and purify chemical products. The temperature and pressure inside the reactor are maintained using several control
loops [50]. In the context of security, the complexity of this process has allowed simulating the realistic behaviour of physical processes under attack [51], [52], [53], [54], [55]. In addition, the simulation-based TEP allows for a low-cost and safe testing of the effect of attacks on physical operation.

We modified the MATLAB/Simulink simulation of the TEP provided by Bathelt et al. [56] by adding blocks to simulate the real-time behaviour of the control network, sensors, actuators, and controllers. We also implemented a Kalman filter-based anomaly detector to estimate process measurements and detect anomalies. A diagram of our testbed is shown in Fig. 5.

The network is divided into four segments connected by a “gateway” router to emulate the distributed nature of modern ICS environments. In the control rooms, where the physical process resides, sensors send measurements over the first network segment to the gateway, which forwards them to the appropriate node on the controllers’ network. The controllers employ a similar procedure to send control signals to the appropriate actuator nodes. The gateway forwards sensor measurements and controller states to the supervisory control room where the anomaly detector and the proposed instantiated framework (indicated as EWS in Fig. 5) reside. The gateway then emulates Remote Terminal Units (RTU’s) which are used to provide an interface between control devices and servers in control rooms.

To simulate the real-time behaviour of sensors, controllers, anomaly detector, and the network we use the MATLAB/Simulink-based TrueTime library [57]. This library has been adopted to study the performance of networked control systems [58], [59], and also in the context of ICS security [60]. The TrueTime library assumes that higher-level network protocols process messages into packets. The TrueTime library simulates medium-access and packet-level network protocols, which are sufficient to study the overhead incurred by the proposed framework.

We compiled the physical process implemented by Bathelt et al. [56] into a MATLAB “mex S-function” to be incorporated in the Simulink-based simulation. We implemented sensor, actuator, and controller codes as TrueTime Kernels, representing the real-time behaviour of control devices with a fixed-priority scheduling policy. The network employs a Carrier Sense Multiple Access with Arbitration on Message Priority (CSMA/AMP) model, which is widely used in industrial Controller Area Network (CAN) bus applications [61]. The TrueTime library assumes that higher-level network protocols process messages into packets.

7.2 Numerical Simulations

7.2.1 Warning Before Harm Occurs

As the objective of our framework is not to detect attacks, but to generate warnings of potential stealthy attacks before harm occurs, we do not consider previous work on attack detection (such as the work surveyed by Giraldo et al. [4]) a suitable baseline to compare our work against. Furthermore, true/false positive metrics, as traditionally defined in the attack detection literature, are not suitable metrics to evaluate our framework, as it is not meant to replace the existing anomaly detector. Rather, our framework’s main utility is in guiding the selection of actions that may reveal a potential intrusion before damage occurs. Therefore, our evaluation demonstrates how our algorithm warns well in advance of potential damage and guides the selection of post-warning actions based on the different thresholds that we designed in Section 6. We perform this evaluation using two attack scenarios conforming to the threat model described in Section 5. This approach is in line with previous work on EWS [7], [25], [27], [29], [35], [62]. For each scenario, we compare the warnings raised by Algorithm 1 to the attack’s ability to cause damage without being detected.

To instantiate the framework, we first approximated the LTI model (1) of the system using a standard system identification technique (nlinmod) in MATLAB. Table 1 shows the safety constraints considered in the present case study, based on the process description provided by Downs and Vogel [48]. We derived an appropriate Kalman filter using MATLAB’s built-in kalman function, and we set an anomaly detection threshold based on a desired false alarm rate of $\beta = 5\%$. Furthermore, we computed the value of the matrix $P$ in Equation (9) for a confidence level $p = 1 - \beta = 0.95$.

In our previous work [15], we performed a detailed evaluation of the accuracy of the safety checking component of Algorithm 1. In particular, we demonstrated how to tune the length of the prediction horizon $K$ to maximise the prediction accuracy. We showed that for the TEP, a $K = 500$, equivalent to $\approx 15$ min into the future, guarantees a high

![Fig. 5. Networked TEP testbed diagram.](image-url)
accuracy in terms of prediction and safety checking. Finally, we set the warnings described in Section 6 to be such that a low criticality warning is issued if Algorithm 1 returns that damage can happen after 250 steps or less, i.e., $\text{SUSP} \geq 0.004$. A high criticality warning is issued if damage can happen after two steps or less with a $\text{SUSP} \geq 0.5$.

The results obtained for the attack scenarios are shown in Fig. 6. For each scenario, we plot the value of the reactor level or pressure, residual, suspicion metric, and warning level over time. Our results can be interpreted as follows:

1) In the first scenario (Fig. 6a), we re-use the same operating conditions and attack described in Section 3. The attack on the reactor starts at $t = 30h$, and the liquids level increases until damage takes place approximately 37 hours later. A high criticality warning is however issued at around $t = 48h$, 19 hours before damage takes place. If we relied only on a proximity-based suspicion metric, we would not be able to detect that the reactor was moving to an unsafe state.

Before the attack starts, a low criticality warning level is maintained most of the time. A high criticality warning is raised after the attack starts, but well before any damage can happen (20 hours). Although a low criticality warning is raised constantly for a long period of time, this does not imply that corrective actions should be taken each time a warning is raised. Indeed, operators can initially collect more data from the concerned area of the system to confirm or refute the hypothesis that an intrusion is present. This data can include network traffic from the concerned area of the system, logs from engineering workstations, PLC configurations - among others. If the hypothesis is refuted yet a low-criticality warning level is maintained, then data collection can either stop or take place periodically in order to make sure that no intrusion is present. This task can be automated using existing dedicated tools [63]. Moreover, we expect the warnings generated by our framework to be correlated with other alerts (e.g., cyber intelligence, insider activity) generated by the EWS. This will provide a more accurate picture of the security situation." For example, these warnings can feed into a Bayesian score similar to the one proposed in [28], [29] to monitor potential network intrusions.

2) In the second scenario, we test the ability of Algorithm 1 to provide warning when the plant is attacked during transient operating conditions. We consider a scenario (Fig. 6b) where the reactor's pressure is steadily brought to lower levels over a long period of time. The attack on the reactor's pressure starts at $t = 70h$, and excessive pressure starts building up in the reactor until damage takes place approximately 18 hours later. A high criticality warning is however issued at around $t = 75h$, 13 hours before damage takes place. Even though the reactor pressure was being lowered throughout the run, Algorithm 1 still identified a state that can be taken to an unsafe operating region through a stealthy attack. If we relied on a purely proximity-based suspicion metric, the reactor's pressure would have appeared to evolve away from an unsafe state.

The scenarios above show that our algorithm can warn well in advance of potential harm and can guide the selection of post-warning actions. We have considered attacks...
We assessed the scalability of Algorithm 1 with respect to (i) the number of safety constraints, and (ii) the length of the prediction horizon $K$ set by operators. For both cases, we averaged the execution time over a 100-hour simulation of the networked TEP, equivalent to $2 \times 10^5$ executions of the algorithm given the sampling time $\Delta t = 5 \times 10^{-4}$ hours $\approx 1.8$ seconds. In addition, for the purposes of performance testing, we modified Algorithm 1 to simulate the worst-case execution scenario where emptiness checks are performed at every predicted state. To test for scalability against the number of safety constraints, we generated random half-spaces representing potential safety constraints. We also fixed the length of the prediction horizon at $K = 500$, equivalent to about 15 mins into the future. For scalability with the length of the prediction horizon, we used the safety constraints in Table 1. Results are shown in Figs. 7 and 8.

The worst-case execution time of the algorithm scales linearly w.r.t. both the number of safety constraints and the length of the prediction horizon. These results prove the ability of the proposed algorithm to scale in safety-critical scenarios, where a larger number of safety constraints are imposed. Furthermore, at $K = 1000$ time steps, equivalent to about 30 min ahead-of-time prediction, the worst-case execution time $\approx 1.3$ sec is less than the sampling period, 1.8 sec, which guarantees a satisfactory real-time response. Note that real-time response can be further improved by performing checks only when the estimated physical and controller states of the system (i.e., the main real-time inputs to Algorithm 1) are undergoing significant changes, i.e., during transient operation. Finally, the algorithm’s worst-case execution time can be improved significantly by considering an implementation in a compiled language such as C rather than an interpreted language like MATLAB.

**Network Overhead.** To assess the effect of the proposed algorithm on the performance of the network, we measured end-to-end time delays at two critical locations in the network: (i) between each sensor and its corresponding controller; (ii) between each controller and its corresponding actuator. For each location, we averaged these measurements over a 100-hour simulation. The values in Table 2 show the average, standard deviation, maximum, and minimum time delays considering all sensors, controllers, and actuators on the network. The proposed algorithm incurs little additional delays on the network. This result is expected since the installation of the proposed scheme requires that only sensor values and controller states are uploaded to the supervisory control room area (Fig. 5). These values are already uploaded to perform anomaly detection in the absence of the proposed framework. It is worth noting that these values are usually uploaded also to process historians for various process control and diagnostics-related logging activities. Therefore, the proposed framework is expected to incur little overhead on the network.

### 7.3 Use Case Scenario

#### 7.3.1 Layout of the ICS

For the purposes of this scenario, we restrict our focus on the reactor stage of the TEP. Namely, we assume that the reactor is housed in a remote control station, the layout of which is inspired by the laboratory experiment performed by Sand [64] and is shown in Fig. 9. The reactor’s temperature controller is installed on a Programmable Logic Controller (PLC), and a Remote Terminal Unit (RTU) is used to interface with the PLC using a specialty software installed on the engineering workstation. The RTU relays control data to the central Supervisory Control And Data Acquisition (SCADA) station, which includes process diagnostics and alarms generated due to possible anomalies.

#### 7.3.2 Attack Scenario

Consider the case of a disgruntled employee looking to cause physical damage to the process. We adapt an attack scenario proposed by Sand [64] which consists of the steps shown in Fig. 9. The employee uses his access credentials to...
enter the reactor room and log onto the engineering work-station. Using his knowledge of the physical process, the employee changes the configuration of the PLC such that false data is slowly injected into the temperature sensor following the stealthy attack described in Section 3. Finally, he leaves the reactor room before damage occurs.

Case 1: Low Criticality Warning. Following a warning of low criticality, relevant data can be uploaded to the main SCADA server to help profile an alleged attack. Fig. 9 shows potential sources of data in low-level devices:

1) Access control device: Access control logs would show that the employee was in the remote station as the warning was issued.

2) Operator workstation/HMI: The HMI of the operator workstation stores logs recording log-on events and issued commands which can reveal the sequence of actions performed by the employee. Vendor-specific software [63] exists to extract and subsequently upload such logs.

3) RTU/PLC: The current control program executing on the PLC triggers events that can constitute an evidence of the attack performed by the employee. Extracting such information from PLC’s without having to power it down is possible, for example, by recording memory variable values using proprietary software such as PLCLogger [63].

By performing this live forensics activity, operators can detect that the employee is initiating a stealthy attack. They may then force the restoration of the PLC configuration and the stored evidence may be used to potentially prosecute the employee in question.

Case 2: High Criticality Warning. A high-criticality warning, such as the one shown in Fig. 6c would typically be followed by measures to prevent a potential incident, in addition to the data collection activities mentioned previously. In the present scenario, such measures could include engaging a trusted backup PLC to handle the control of the reactor instead of the one with the potentially malicious configuration; or temporarily disabling the RTO module.

7.4 Discussion

Before concluding this paper, we make some final remarks regarding both the usefulness of the framework and potential practical deployment issues.

7.4.1 Supporting ICS Forensics

Recently, an increasing body of work has considered forensics in ICS [63], [65], [66], [67]. In these systems, the low processing power of low-level devices such as sensors and actuators limits the deployment of event-logging tools. In addition, the process’ safety criticality limits the degree of interference of forensic tools with the system. It is also often impossible to shutdown an ICS to perform post-mortem forensics, which forces operators to rely mainly on live forensics methods [67].

The proposed framework can support live forensics by triggering data collection activities only when a warning about potential damage to equipment is raised. This selective data collection activity, as illustrated in the previous use case scenario, reduces the overhead for the network and the low-processing devices. In addition, measuring grounds for suspicion in real-time reduces the risk of losing evidence about a stealthy attack, in case this attack causes damage to the ICS sensors and/or actuators.

Furthermore, note that in the scenario described previously, the attacker did not need to break into the network or take advantage of a software vulnerability. An EWS relying only on indicators based on network events may not be able to warn well in advance of such an attack. Our framework can complement an EWS that monitors insider activity (e.g., [24]) by warning when such activity targets the physical components and may cause damage.

7.4.2 Potential Limitations

First, the configuration of our framework may require some manual effort. However, we remark that approximate mathematical models of the system, its anomaly detector, and unsafe operation are standard in control engineering. Second, to alleviate the computational cost incurred by reachability analysis, we computed approximate symbolic reachable sets offline and instantiated them at runtime — an approach inspired by simplex control architectures [11]. We realise nonetheless that the reachability tools we used in the present case study are specific to LTI systems. To increase generalizability of our results, in future work we
will explore adoption of a different set of tools to instantiate our framework to different types of systems. Finally, to reduce the risk of a potential adversary subverting the EWS, one possible solution is to implement it on a Shadow Security Unit (SSU) as proposed by Graveto et al. [68]. Such devices are computers designed specifically to remain hidden from potential offenders. Encryption mechanisms can also be added as an extra layer of security, to favour more secure communications at the potentially reduced cost of performance.

8 Conclusion

In this paper, we considered the problem of stealthy attacks on safety-critical ICS. We proposed a framework which can be used as part of an EWS to raise early warnings based on grounds for suspicion representing “physics-based” preliminary indicators of a stealthy attack. We defined two grounds for suspicion based on the physical dynamics of a system: (i) feasibility of a stealthy attack and (ii) proximity of the system to unsafe operating regions. To monitor the grounds for suspicion in real-time, we proposed a suspicion metric based on a mathematical model of the system. We also provided soundness principles to ensure that the metric is consistent with the measured grounds. To illustrate our framework, we considered the case of a safety-critical chemical reactor system faced with a stealthy attack on its sensors. We adapted reachability tools from the literature, namely ellipsoidal calculus, to evaluate the suspicion metric efficiently in real-time. We also illustrated with a use case that our framework can support live forensics activities, by triggering early evidence collection and preserving potential evidence about a stealthy attack.

Going forward, we aim to apply our framework to different systems and attacks. We will consider other existing threat models and modelling frameworks for the physical process. We will also implement a prototype tool to reduce the human effort required to instantiate our framework to a specific system. In addition, we will investigate in more detail the ability of different attack scenarios to cover the space of the considered attack models in the context of evaluating different instances of the proposed framework. Finally, we will further investigate the applicability of our work to ICS forensics.

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