PyMORPH: automated galaxy structural parameter estimation using PYTHON

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ABSTRACT

We present a new software pipeline – PyMORPH – for automated estimation of structural parameters of galaxies. Both parametric fits through a two-dimensional bulge disc decomposition and structural parameter measurements like concentration, asymmetry etc. are supported. The pipeline is designed to be easy to use yet flexible; individual software modules can be replaced with ease. A find-and-fit mode is available so that all galaxies in an image can be measured with a simple command. A parallel version of the PyMORPH pipeline runs on computer clusters and a virtual observatory compatible web enabled interface is under development.

Key words: techniques: photometric – galaxies: fundamental parameters – galaxies: photometry – galaxies: structure.

1 INTRODUCTION

In recent years, the morphological analysis of galaxies has provided invaluable information regarding their origin and evolution. This analysis used large galaxy samples drawn from modern astronomical surveys such as the Sloan Digital Sky Survey (SDSS; York et al. 2000; Abazajian et al. 2009), Two Micron All Sky Survey (2MASS; Skrutskie et al. 2006), GEMS (Rix et al. 2004), Cosmic Evolution Survey (COSMOS; Scoville et al. 2007) etc. Since visual estimation of galaxy morphology is most accurate, it is widely used. However given the large numbers of galaxies in astronomical data sets, it is impractical to classify them all using human classifiers (unless a large volunteer base is available, like in the GalaxyZoo project (Lintott et al. 2008). Besides, different human classifiers may not agree completely on the morphological classification. It is therefore desirable to develop a reliable, objective and automated method for quantitative morphological classification.

It has been known for a long time that the visual morphology of galaxies is well correlated with their physical properties. For example, the colour correlates with the morphology such that late-type spirals are bluer, on average, than elliptical galaxies. Similarly, we can make use of the surface brightness profile of galaxies to classify them.

In general, the stellar component of galaxies can be decomposed into a bulge and a disc. While the disc profile is usually an exponential, the bulge is well approximated by the Sérsic function (Sersic 1968). It is found that the bulge-to-total luminosity ratio \(B/T\) of galaxies correlates with the visual morphology, where the \(B\) is the light contained in the bulge component and \(T\) is the total light of the galaxy. Elliptical galaxies are expected to have \(B/T\approx 1\), while pure disc galaxies have \(B/T\approx 0\). In recent years, most researchers prefer to fit a two-dimensional (2D) representation of the bulge and disc profiles directly to a broad-band image of the galaxy (Byun & Freeman 1995; de Jong 1996; Wadadekar, Robbason & Kembhavi 1999; Peng et al. 2002; de Souza, Gadotti & dos Anjos 2004). This structural decomposition technique is not only useful for quantifying the morphology but also an excellent tool for studying the formation and evolution of galaxies of different morphological types (e.g. Khosroshahi, Wadadekar & Kembhavi 2000; Ravindranath et al. 2001; Simard et al. 2002; MacArthur, Courteau & Holtzman 2003; Barway et al. 2007, 2009; Vikram et al. 2010). Recent research has shown that the simple Sérsic bulge + exponential disc formulation is not adequate for many galaxies (Laurikainen, Salo & Buta 2005; Gadotti 2008; Peng et al. 2010) and fitting these simple models can lead to wrong estimates of structural parameters. Nevertheless, these simple models, when used appropriately, do give reliable results and are useful indicators of galaxy structure.

Since parametric methods (such as the 2D bulge disc decomposition) are generally computationally intensive and difficult to apply to small faint galaxies, several non-parametric methods have been developed during the last few years to quantify galaxy morphology. The main motivation for the development of these non-parametric methods is to make classification possible at very high redshifts where the images do not have enough resolution elements and signal-to-noise ratio for visual classification (Abraham et al. 1996;
Conselice 2003; Lotz, Primack & Madau 2004). Non-parametric methods are not computationally intensive compared to the parametric methods. However, with non-parametric methods, it is not easy to convert measured quantities to physically meaningful parameters such as bulge or disc luminosity.

In this paper, we describe an automated pipeline software PyMORPH to estimate structural parameters of galaxies. We have developed this pipeline by glueing together widely used codes such as SExtractor (Bertin & Arnouts 1996) and GALFIT (Peng et al. 2002)\(^1\) to our own codes for automation and quality control. We have also developed our own implementation of non-parametric methods (Section 2). In Section 3, we explain the operational procedure to obtain structural parameters using GALFIT and SExtractor. In Section 4, we describe how to setup the pipeline for the parametric and non-parametric methods. In Section 5, we describe the results of the simulations we have done to test the reliability of the pipeline. Finally, we describe a multiprocessor implementation of PyMORPH and its performance characteristics (Section 6).

2 NON-PARAMETRIC METHODS
IN PyMORPH

We have implemented an automatic procedure for structural decomposition of galaxies using GALFIT supplemented by measurements using non-parametric methods. The algorithms we use to estimate non-parametric quantities are described in Conselice (2003) and Lotz et al. (2004). For completeness, we summarize the main features of these algorithms. For the calculation of all non-parametric quantities we use the sky value and centre as determined by SExtractor, wherever required. Furthermore, we use the SExtractor source catalogue to identify and mask neighbour objects.

### 2.1 Concentration index (C)

Concentration is defined as the ratio of the radius of the galaxy which contains 80 per cent of the total light (\(r_{20}\)) to the radius of the galaxy which contains 20 per cent of the total light (\(r_{20}\)), i.e.

\[
C = 5 \log \left( \frac{r_{80}}{r_{20}} \right).
\]

(1)

Here, the total light of the galaxy is taken to be the light within 1.5 times of the Petrosian radius \(r_p\) (hereafter extraction radius, \(R_T\)), where \(r_p\) is the radius of the galaxy at which the Petrosian parameter \(\eta\) takes a value of 0.2. The Petrosian parameter is defined as follows:

\[
\eta = \frac{\langle L_r \rangle}{\langle I_r \rangle},
\]

(2)

where \(\langle L_r \rangle\) is the average light at the radius \(r\) and \(\langle I_r \rangle\) is the average light inside \(r\). Near the centre of the galaxy, where the light profile changes rapidly, we need to oversample the pixels to obtain an accurate measurement. We achieve this by subpixelization inside the central 7 pixels (radius) of the galaxy by a factor of 10.

### 2.2 Asymmetry (A)

We calculate asymmetry using the algorithm devised by Conselice (2003). The steps are as follows: we rotate the galaxy through 180° about its centre which is taken to be the centroid (first image moment) of the galaxy pixels. We use bilinear interpolation to obtain the rotated image. In the next step, we subtract the rotated image from the original image of the galaxy. From the residual image we estimate the total residual flux inside the extraction radius. This is then normalized by the total flux of the galaxy. This step can be represented as follows:

\[
A_0 = \frac{\sum |I_O - I_R|}{\sum I_O},
\]

(3)

where \(I_O\) and \(I_R\) are original image and the rotated image, respectively, and the summation is over all valid pixels excluding the pixels contaminated by light from neighbouring objects, inside the radius \(R_T\). In the next step, we identify possible biases in the measured asymmetry value and correct for them. The first bias to the estimated asymmetry value is due to the uncertainty in the estimated centroid of the galaxy. For example, a perfectly symmetric galaxy can give non-negligible asymmetry value if we cannot determine the centroid of the galaxy exactly. To correct for this bias we minimize the asymmetry with respect to the centre. To do that, we create a square grid of nine points which includes the initial centroid of the galaxy. The bin width of the grid of points is a fixed fraction of the half light radius of the galaxy (0.01\(r_{50}\)). We find asymmetry of the galaxy about all these nine points, and assign the point corresponding to the minimum asymmetry as the new centroid of the galaxy. We then generate a new grid of points described as above, find the asymmetry of the galaxy about this newly created grid of points and again determine the minimum asymmetry. This process continues until we reach a stable point where the asymmetry is minimum about that point compared to the estimated asymmetry of the galaxy about the neighbouring points. This process is illustrated in Fig. 1 (Conselice 2003).

The second bias is introduced by the gradient of the sky near the object. To compensate for this, we estimate asymmetry of the sky and subtract it from the object asymmetry. To get the background asymmetry we find an empty region near the object, which should represent the real sky at the object position, and therefore, cannot be far from the object. On the other hand, it is difficult to get an empty sky region very near to the object. This forces us to use

\[\text{Figure 1. The centring correction in asymmetry measurement applied to galaxy NGC 5585. The red square shows the initial estimate of the centroid of the galaxy and the red circles represent the grid points. The blue square represents the new centroid and the blue circles correspond to the points on the new grid. The grids are magnified five times, for illustration.}\]
an optimum distance from the object centre to search for the sky region. (This distance is same as the dimension of cut-out of the object. We explain this in Section 3.2.) We mask all the objects in the cut-out and estimate the sky standard deviation ($\sigma_{\text{sky}}$). Then, to identify a region of blank sky within the cut-out, we put a square region at the bottom left-hand corner of the cut-out with a size $X$. We find that $20 \leq X \leq 30$ pixels is optimal to get background asymmetry. Inside the square region identified as possible blank sky, we check how many pixels are within $\pm N\sigma_{\text{sky}}$. Initially, we take $N = 1$. If we cannot find at least 80 per cent of the pixels within this range we slide the square by 2 pixels along the $x$-axis and repeat the procedure. If we do not find a suitable blank sky region, this process continues until we hit the image boundary. Then we slide the blank sky search square along the $y$-axis. If we fail to find a region after searching the whole image, we assume that the sky has a large gradient. Therefore we increase $N$ by 1.3 times and search sky region inside $\pm N\sigma_{\text{sky}}$ as we did earlier. This simple approach may fail when we have a highly crowded field. In such situations, $\text{PyMorph}$ notifies the user of the problem by setting the proper flags. This process is summarized in Fig. 2.

After we find an empty sky region we mask all pixels with counts outside $\pm N\sigma_{\text{sky}}$ and find the asymmetry of that region and minimize it in the same way as we did in the case of the object. Finally, we subtract the minimized background asymmetry from the minimized object asymmetry to get the ‘true’ asymmetry which can be represented as

$$A = \min(A_O) - \min(A_B),$$

where $A_O$ is the composite asymmetry of both object and sky, $A_B$ is the asymmetry of the sky and $A$ is the true asymmetry (Conselice 2003).

### 2.3 Clumpiness ($S$)

The clumpiness $S$ is a quantitative measure of clumpy regions in the galaxy. These are associated with star-forming regions and thus clumpiness of spiral galaxies is larger, on average, than that of elliptical galaxies. To find $S$ we convolve the galaxy image with a boxcar function of width $0.25r_p$, where $r_p$ is the Petrosian radius of the galaxy. This smoothed image is then subtracted from the original image and the residual is summed within the extraction radius. During this process, we mask the central part of the galaxy as those regions are unresolved. The output of this process is the sum of the clumpiness of the object and background. To get the clumpiness of the object alone, we find the background clumpiness and subtract it from the composite value. The background region used for this purpose is same as that used for the asymmetry calculation. The whole process can be summarized in the following equation:

$$S = 10 \left[ \frac{\sum I_O - I_S}{\sum I_O} - S_B \right],$$

where $I_O$ is the original image, $I_S$ is the smoothed image and the summation is over all the positive pixels of residual image with the annular region of width $0.2R_T \leq r \leq R_T$. $S_B$ is the clumpiness of the background region (Conselice 2003).

### 2.4 Gini coefficient ($G$)

It has been found that the Gini coefficient $G$ is a powerful way to describe the morphology of a galaxy (Lotz et al. 2004). This coefficient can be regarded as a generalized concentration parameter. If all the light in the galaxy belongs to a single pixel, the Gini coefficient takes a value of 1. On the other hand, if the total light distributes uniformly among all the pixels belonging to the galaxy,
then the Gini coefficient will be 0. On average, an elliptical galaxy has a larger Gini coefficient than a disc galaxy.

To get G we need to find the pixels in the image which belong to the galaxy, i.e. obtain the segmentation map of the galaxy. This is important as G will be underestimated if we include sky pixels and will be overestimated if we miss the outer pixels of the galaxy. To determine which pixels belong to a galaxy, we convolve the galaxy image with a boxcar filter of size \( r_0/5 \). This process will increase the signal-to-noise ratio in the outer parts of the galaxy. Then we measure the surface brightness \( I_p \) at \( r_0 \). We assign all the pixels in an image with \( I_p \leq I \leq 10r_0 \) to the galaxy, where \( \sigma \) is the standard deviation of the sky. The upper limit ensures that no cosmic rays or spurious pixels are included in the segmentation map. Then the pixels belonging to the segmentation map are sorted according to their photon count \( I_i \) and \( G \) is calculated using the equation:

\[
G = \frac{1}{I_n(n-1)} \sum_{i=1}^{n} (2i - n - 1)|I_i|, 
\]

where \( I_i \) is the photon count in the pixel \( i \) which belongs to the segmentation map, \( I_n \) is the mean of all the pixel values \( I_i \) and \( n \) is the total number of pixels (Lotz et al. 2004).

### 2.5 Second-order moment of the brightest pixels (M20)

This quantity gives an idea of how the brightest pixels are distributed over the galaxy segmentation map. For elliptical galaxies, the brightest pixels are concentrated near the centre of the galaxy. Therefore, the M20 parameter will be smaller for ellipticals compared to spiral galaxies where we observe large number of star-forming regions distributed all over the galaxy. To compute M20 we use the segmentation map generated to estimate the Gini coefficient. We start by computing the flux-weighted second-order moment of the galaxy \( M_T \) as

\[
M_T = \sum M_i = \sum I_i \left( (x_i - x_c)^2 + (y_i - y_c)^2 \right),
\]

where \( I_i, x_i \) and \( y_i \) are the flux value and \( x \) and \( y \) coordinates of the \( i \)th pixel in the segmentation map and \( x_c \) and \( y_c \) are the initial centre of the galaxy. We then minimize \( M_T \) with respect to the centre of the galaxy as the initial value of the centre is the centroid of the galaxy. In the next step we sort the pixels according to their flux value and find the moment of the 20 per cent brightest pixels of the galaxy using the equation:

\[
M_{20} = \log \left( \frac{\sum M_i}{M_T} \right).
\]

where the summation continues until it satisfies \( \sum I_i \leq 0.2I_T \), where \( i \) is the pixel in the sorted array of the segmentation map and \( I_T \) is the total light of galaxy (Lotz et al. 2004). It can be seen that when calculating \( M_{20} \) the pixels are weighted by \( r^2 \) which results in a large \( M_{20} \) value for galaxies with many star-forming regions distributed away from its centre. Therefore, \( M_{20} \) will be smaller for passbands which map the underlying old stellar distribution [e.g. near-infrared (IR)] than those which map the young stellar population [e.g. near-ultraviolet (UV)].

### 3 ESTIMATING STRUCTURAL PARAMETERS OF GALAXIES

Many well tested codes are available to perform 2D decomposition. These include FITGAL (Wadadakar et al. 1999), GIM2D (Simard 1998), GALFIT (Peng et al. 2002), BUDDA (de Souza et al. 2004) etc. Although the basic working principles of these codes are the same, they implement different minimization algorithms. FITGAL uses the Davidson–Powell–Fletcher minimization algorithm as implemented in the MINUIT code developed at CERN (James 1994) while GIM2D minimization uses the Metropolis algorithm. Marquardt–Levenberg minimization drives GALFIT and BUDDA uses a multidimensional downhill simplex method (Press et al. 1992). Because of the complexity of the parameter space it is very important to carefully setup the minimization so that these codes find the global minimum, as far as possible. In PyMORPH, we have chosen to use GALFIT for 2D decomposition because of its simplicity and faster convergence. However, the pipeline is designed in a modular way so that the minimization engine can be easily changed at a future date, if required.

The main preparatory steps before running GALFIT are the following: (1) detect objects in the input image and obtain their photometric parameters using SExtractor; (again, the pipeline can be easily modified to use another source extraction software); (2) create a cut-out of the main object; (3) create an appropriate mask image to reject neighbour objects and spurious pixels; (4) create a configuration file for GALFIT. Besides 2D fitting, PyMORPH also performs the following tasks for every galaxy that it fits: (1) generates a one-dimensional (1D) profile of input and best-fitting model galaxy using the IRAF/STSDAS ellipse task to facilitate visual checks for obvious fitting errors; (2) converts all the fitted parameters to physical parameters using the user specified cosmology and the galaxy redshift (if available); (3) creates outputs in several formats which includes CSV and html and stores results in a mysql database; (4) creates diagnostic plots in png format (see example in Fig. 3).

### 3.1 Object detection and photometry

This is the initial stage of PyMORPH. We use SExtractor to detect objects in the input image and perform photometry on them. The input image may either be a large frame or a cut-out of the galaxy of interest. If the image is a large frame, the astronomer may be interested only in a few specific objects in the frame or may want to generate parameters for all galaxies in the frame that satisfy some selection criteria. In either case, before proceeding, a catalogue with the exact location and magnitude of the objects of interest is needed. To obtain such a catalogue, PyMORPH runs SExtractor on the input image to generate a SExtractor photometric catalogue. The SExtractor output parameters used by PyMORPH are \( X_{\text{IMAGE}}, Y_{\text{IMAGE}}, \text{ALPHA_SKY}, \text{DELTA_SKY}, \text{FLUX_RADIUS}, \text{THETA_IMAGE}, \text{A_IMAGE}, \text{ELONGATION}, \text{ISO0}, \text{BACKGROUND}, \text{CLASS_STAR} \) and \( \text{MAG_AUTO} \). \( X_{\text{IMAGE}} \) and \( Y_{\text{IMAGE}} \) are the \( x \) and \( y \) coordinates, respectively, of the centroid of the object in pixel units. \( \text{ALPHA_SKY}, \text{DELTA_SKY} \) are the RA and Dec. of the object. \( \text{FLUX_RADIUS} \) is the half light radius. \( \text{THETA_IMAGE}, \text{A_IMAGE}, \text{ELONGATION} \) represent the position angle, the semi-major axis length (a) and ratio of the semimajor to semiminor axis length of the object. SExtractor divides the detected objects into eight isophotal levels above the ANALYSIS_THRESH. ISO0 represents the area of the object above the ANALYSIS_THRESH in units of pixel\(^2\). MAG_AUTO, BACKGROUND and CLASS_STAR are the magnitude, background value at the object position and the stellarity parameter of the object. The user can choose the SExtractor local or global background. CLASS_STAR = \( \sim 1 \) for a star and \( \sim 0 \) for a galaxy.

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3.2 Position match and object cut-out generation

After the SExtractor catalogue is created, the program compares the user given input catalogue of objects (which lists the galaxies of interest) with the SExtractor catalogue. For each object in the input catalogue, Pymorph finds the corresponding entry in the SExtractor catalogue either by matching the RA and Dec. coordinates or by matching pixel coordinates. The matching radius can be set by the user, either in units of pixels or in arcsec. For every successful match between the input catalogue and the SExtractor catalogue, Pymorph reads all the required SExtractor photometric parameters of that object for further use.

The next step is to create a cut-out image of the object to feed to GALFIT. The size of the cut-out image should be such that it contains enough sky pixels without becoming very large in size. The first criterion is highly desirable as insufficient number of sky pixels may cause incorrect background estimation by GALFIT. This will seriously affect the estimation of Sérsic index of the bulge. On the other hand, including a large sky region in the cut-out will increase computational resource requirements. We use the SExtractor FLUX_RADIUS (\(R_\text{f}\)), ELONGATION (\(a/b\)) and THETA_IMAGE (\(\theta\)) parameters to find the optimum size of the cut-out as follows:

\[
\begin{align*}
X = F_{\text{rad}}R_{50} (|\cos \theta| + \frac{b}{a} |\sin \theta|), \\
Y = F_{\text{rad}}R_{50} (|\sin \theta| + \frac{a}{b} |\cos \theta|),
\end{align*}
\]

where \(X\) and \(Y\) are the dimension of the cut-out centred on the galaxy centre and \(F_{\text{rad}}\) is a user specified parameter. Through trial and error, we found that \(F_{\text{rad}} = 6\) gives optimum size for the cut-out image. Using the size and the centroid parameters of the object, we cut the portion of image and the corresponding weight image (if available).

3.3 Create mask image

An advantage of GALFIT is that it allows us to simultaneously fit any number of objects. However it is not advisable to fit many objects simultaneously as that increases the number of free parameters. In such situations, the fit may converge to a local minimum. Therefore, we should simultaneously fit for a neighbouring object only if it is large and/ or bright enough to significantly contaminate the main object. To decide whether a neighbouring object should be included in the simultaneous fitting, we use the \(A_{\text{IMAGE}}\), ISO0 parameters of each object. We compare the parameters of all neighbouring objects in the SExtractor catalogue with those of the object of interest. We check whether the objects overlap with the main object by comparing their scaled semimajor axis (the scale is user specified). The scale determines the distance to the closest neighbour to be fitted simultaneously with the object. For example, let us say that the distance between the centres of the object of interest and its neighbour is 100 pixels, the semimajor axis of the object of is 60 pixels and that of the neighbour is 30 pixels. Then, even if the galaxies have circular shape they will not overlap (because \(60 + 30 < 100\)) and the neighbour will therefore be masked. If the user requires that such neighbours be fitted simultaneously, the scale parameter can be tweaked. If the scale parameter is set to 2, then \((60 + 30) \times 2 > 100\) and now the neighbour will be fitted simultaneously with the object. If the program finds overlapping neighbours, it also checks whether the area of the neighbour is larger than a user specified fraction of the main object. If the area (ISO0) of the neighbour is higher than a threshold fraction of the area of the object of interest, then it will be fitted simultaneously. If the neighbour’s area is below the threshold fraction, then that neighbour will be masked irrespective of its distance from the object. Therefore the condition for simultaneous fitting is as follows:

\[
d < T_{\text{g}}(R_{\text{n}} + R_{\text{a}}), \quad A_{\text{n}} > T_{\text{a}}A_{\text{o}},
\]

![Image 1](https://example.com/image1)

![Image 2](https://example.com/image2)

**Figure 3.** Diagnostic output from Pymorph. The top left-hand panel shows the image of the galaxy, top middle panel shows the best-fitting model image and the top right-hand panel shows the residual (difference between galaxy and model) image after the fit. Lower left-hand panel shows the 1D profile comparison of original (as data points) and model (as a solid line) for the galaxy. The lower middle panel shows the difference between the 1D profiles of input and model galaxy. The lower right-hand panel shows the histogram of the residual image, with the best-fitting Gaussian overplotted in red.
where $d$ is the distance between object and neighbour, and $R_o, R_n$ are the A_IMAGE parameters and $A_o$ and $A_n$ are the ISO0 parameters of object and neighbour, respectively. $T_R$ is a user specified parameter which decides the threshold fraction of overlap between object and neighbour. The value of $T_R$ decides the smallest object which is to be included in the simultaneous fit with the object of interest. We found the control parameters $T_R = 3.0$ and $T_A = 0.3$ give good results. Neighbours which do not satisfy the simultaneous fit criterion in equation (10) are masked out. To do this, PyMORPH creates an elliptical mask at the position of the object. This mask has the same ellipticity as that of the neighbour but its semimajor axis is scaled by an amount $T_M$ which is also to be specified by the user, i.e. the semimajor axis of the mask becomes $T_M R_n$. This process continues for all the objects in the SExtractor catalogue and finally we have a mask image that is the union of masks for all the contaminating objects. The block diagram describing this process is shown in Fig. 4.

This masking technique works only if SExtractor detects the neighbouring object, in the first place. Since that process depends on the DETECT_THRESH and DETECT_MINAREA parameters the user chooses, it is possible that some spurious pixels bright enough to affect the fit may be left undetected by SExtractor. So, we use the following simple technique to mask such pixels. From the centre of the main object, we make elliptical annuli with increasing radii. In the inner aperture we find the maximum value of the galaxy. We assume a smooth light distribution for the galaxy which decreases with distance from the centre. This implies that the largest value in the central elliptical aperture is the maximum value the object can have. So, we mask all the other pixels outside the inner aperture with value greater than this maximum value. Now we go to the next pair of annuli and find the maximum and mask other pixels outside this aperture which have value larger than the maximum of this aperture. This procedure continues till the aperture radius hits the image limit. Using this technique we are likely to mask small regions with a high flux e.g. knots of star-forming regions in spiral arms. However, since we are attempting to determine global parameters for the bulge and disc of the galaxies, masking out local fluctuations over the underlying bulge and disc will likely only improve the parameter estimation. However, if desired, one can switch off this masking technique setting the ‘mask-norm’ option. In that case, only the neighbour objects will be masked. Now, almost all the spurious pixels which may be part of undetected objects should be masked correctly. We combine this mask image with the mask image made using the SExtractor catalogue to get the final mask.

3.4 Create configuration file for GALFIT

GALFIT configuration can be done either through a text file or through the command line. PyMORPH creates an input configuration file for each object in the user given catalogue to feed GALFIT. This file specifies the filenames of the input image, the weight image and the point spread function (PSF) image. The other entries include initial values of the parameters of the components used in the fitting. For 2D decomposition, a galaxy is usually assumed to have, at least, a bulge and a disc component. The bulge is modelled by a Sérsic function of the form

$$I(r) = I_e \exp \left( -b_n \left( \frac{r}{r_e} \right)^{1/n} - 1 \right),$$

where $I(r)$ is the intensity of the bulge at radius $r$, $I_e$ is the intensity of the bulge at radius $r_e$, $r_e$ is the half light radius and $n$ is the Sérsic index of the bulge. $b_n$ is a quantity which depends on $n$. Similarly, the disc part is usually modelled using the exponential form

$$I(r) = I_d \exp \left( -\frac{r}{r_d} \right),$$

where $I_d$ is the disc intensity at the centre and $r_d$ is the disc scale-length. The surface brightness profile of the galaxy is modelled as a linear combination of these two functions.

There are more than a dozen parameters to be fitted during the decomposition of a galaxy. These include the centres of bulge and disc components and their total magnitudes, scale radii, axial ratio and position angles. Sérsic index of the bulge is another parameter...
involved in the fitting. GALFIT offers two additional parameters which model the boxiness/disciness of the bulge and disc. We have not used these parameters in our fits. Apart from the parameters involved in the photometric components of the galaxy, one other important parameter is the sky. There is an option in GALFIT to fit sky with gradient in x and y directions of the image. To increase our chances of finding the global minimum from GALFIT, we need to set the appropriate initial values for the fit parameters. We use SEXTRACTOR MAG_AUTO and FLUX_RADIUS parameters of the galaxy as the initial values for the total magnitudes and scale radii of both bulge and disc. The initial values of the axis ratios of both bulge and disc are set from the SEXTRACTOR ELONGATION parameter and position angle is calculated from THETA_IMAGE. We always set the initial value for the Sérsic index $n$ to 4. The sky parameter is set to the SEXTRACTOR value. We found that SEXTRACTOR slightly overestimates the background value which can result in incorrect estimation of bulge parameters. This issue will be discussed in Section 5.1. The working of PyMorph is summarized as a block diagram in Fig. 5.

4 SETTING UP PyMorph

PyMorph is written entirely in the PYTHON programming language. PYTHON is a modern, high-level programming language with many features that encourage readable and reusable code. Several current astronomical data analysis systems have been made accessible through PYTHON (e.g. IRAF for IRAF and CASA.PY for AIPS++). PYTHON will play a major role in many new software initiatives in astronomy.

Besides the standard PYTHON modules, additional modules required by PyMorph are NUMPY, MATPLOTLIB and PYFITS. NumPy is used for arithmetic manipulations on the image array and matplotlib is used to generate output plots. PYFITS is a PYTHON module to read and write fits images. As we have already mentioned, SEXTRACTOR and GALFIT currently serve PyMorph as the detection and fitting programs. Since all the required processing for 2D decomposition is pipelined, the user needs to initialize the code correctly so that it completes without needing further intervention. All the required input parameters can be set through an input configuration file. Some parameters can be given to PyMorph via command line as well. An example input configuration file for PyMorph is shown in Fig. 6.

There are 12 blocks in the configuration file. Most of the parameters in blocks A and B are self-explanatory. The parameter psflist corresponds to a file containing the list of suitable PSF images. These may be stellar images from the input frame (typically unsaturated, isolated bright stars) which the user feels are accurate representations of the PSF. It is known that in large frames the PSF may vary spatially. Therefore the general principle is to use the nearest star to the object as the PSF. If the names of these stellar images follow the convention psf_RaDec.fits, e.g. psf_1216382-1200443.fits, then PyMorph will automatically find the nearest PSF to the object from psflist and use it for fitting, otherwise it assumes that there is a one to one correspondence between the list of PSFs and galaxies to be fitted. The thresh_area and threshold parameters in block D correspond to $T_R$ and $T_A$, respectively, in equation (10). mask_reg ($T_M$) determines how much area of the neighbour should be masked.

The size keyword is a list of five parameters which control the size of the cut-out image. The first one in the list is a flag that tells the program to create a cut-out of the object. This is needed sometimes when the user already has a cut-out of the objects. In those situations, this parameter should be unset. Using the second entry in the list, the user can set the size of the cut-out of all the objects fixed at a particular value irrespective of the real size of the object. If the user wants to create cut-out of objects scaled by their angular size, the size of the cut-out will be determined by the third parameter in the list. This is the quantity $F_{cut}$ involved in equation (9). The fourth quantity determines shape of the cut-out. If the user sets the parameter, then the cut-out will have a square shape with size equal to the maximum of $X$ and $Y$ which is given by the equation (9). Otherwise the cut-out will have rectangular shape.
of size X and Y. The final entry in the list is used if the user does not set the second entry e.g. an entry size = [1, 1, 6, 1, 120] tells the program to create a cut-out, measure size from the objects, that the size should be six times larger than the half light radius of the objects and to make a cut-out of square shape. On the other hand, if the user sets the size keyword as [1, 0, 6, 1, 120], then the program will create a cut-out of size 120 \times 120 irrespective of the size of the galaxy.

The parameter searchrad is the search radius used to match the input catalogue with the SExtractor catalogue. The comparison can either be in pixels or in arcsec. Therefore if the user set searchrad = '0.3arc' then the program matches objects within 0.3 arcsec. On the other hand, the entry searchrad = '5pix' matches objects within 5 pixels. The cosmological parameters in the block F will be used to convert the fitted parameters to physical units. The G block parameters will be used for the calculation of asymmetry of objects. Through back_extraction_radius parameter the user can set the size of the background region which will be used to find the asymmetry of the background. The parameters in block H determine the different modes of PyMORPH behaviour. gcut should be set if the user

Figure 6. Sample input configuration file for PyMORPH.
wants to supply cut-outs of galaxies. *decompose* and *cas* should be set to get parametric and non-parametric results, respectively, from PyMorph. The *findandfit* is implemented in order to get the structural parameters of all the objects in large frame(s) which satisfy some user defined criteria. For example, this mode can be used if the user wants to generate the structural parameters for all objects in a frame between magnitudes $m_1$ and $m_2$. If *crashhandler* is set then the program automatically reruns *GALFIT* for some obvious fitting errors. In the presence of a bright neighbour or dust lanes in the galaxy, the best-fitting centre of either bulge or disc can be significantly different from the optical centroid of the galaxy. PyMorph tracks errors at all the stages of the pipeline and saves those errors as flags. Therefore it is possible to identify the stages of the pipeline that have failed, in some way. The obvious fitting errors include incorrect centres, i.e. the fitted centre of the component is very far from the visible centre of the galaxy, or some parameters have hit the limit of their allowed range. After a fitting process finishes, PyMorph checks for these errors. If the program finds an incorrect centre, the galaxy is refit with tight constraints on the range of centre. If the program finds a parameter that hits the limit, then it increases the fitting range and carries out a refit, which may give a better result. If the refit also fails, the galaxy is flagged as a poor fit (indicated in the FIT parameter in the output catalogue). Finally, the *repeat* mode is implemented to rerun PyMorph semi-automatically. It is possible that *GALFIT* converges to a local minimum for a few galaxies. Then the user can edit the corresponding *GALFIT* configuration file, mask etc. to rerun *GALFIT* again, if the pipeline is set to run in *repeat* mode. PyMorph generates all the necessary intermediate files to do decomposition which includes the mask, *GALFIT* configuration files etc. and saves them to disk. If the user finds that *GALFIT* failed to converge to a global minimum because of improper initial values of the parameters or a poor mask image, then the user can manually edit the mask image or slightly alter the *GALFIT* initial values. After this, the user can set the repeat mode and run *PyMorph*. In that case, *PyMorph* uses the existing intermediate files to run *GALFIT* without generating them anew.

The I block parameters control *GALFIT*. Through *components* keyword the user can set the number of photometric components of galaxies for fitting. If *components* = ['bulge', 'disc'], then a Sérsic and an exponential function will be fitted to the galaxy’s surface brightness. Through *fitting* the user can fix/free the centres of the fitting functions and sky. For example, *fitting* = [1, 1, 0] tells the program to set the centres of the bulge and disc as free parameters and fix sky at the initial value during fitting. The program reads the location of SExtractor, *GALFIT* and *PyMorph* from the J block. The K block parameters will be used to determine whether a given fit is acceptable or not. This includes the simple reduced $\chi^2$ (chisq) and center deviation. center deviation is a measure of the difference between the initial and fitted centres of the components in pixel units. If this difference is greater than center deviation, then the corresponding fit will be considered as bad. This will be refitted with tight constraints on the centres provided the user has set crashhandler parameters in the H block. The final L block deals with the output data base. If the program finds a mysql data base server then these parameters become active. All other parameters in this block are self-explanatory other than dbparams. Through dbparams the user can create additional columns in the data base table and set their values. For example, *dbparams* = ['Cluster:cl1216-1201', 'ObsID:1:int'] will create two additional columns Cluster and ObsID in the current data base table. The functions of different blocks in the PyMorph configuration file are summarized in Table 1.

### Table 1. Functions of different blocks in the PyMorph configuration file.

| Block | Function |
|-------|----------|
| A     | Input images and catalogues |
| B     | Output files |
| C     | PSF file |
| D     | Masking conditions |
| E     | Cut-out size |
| F     | Cosmology |
| G     | CASGM parameter measurement |
| H     | Fitting modes |
| I     | GALFIT controls |
| J     | Set path to software |
| K     | Classification criteria |
| L     | Data base information |

## 5 TESTING THE ROBUSTNESS OF PyMorph

### 5.1 Caveats of pipeline use

Before we describe the tests we carried out to examine the robustness of the PyMorph pipeline, we would like to caution the user against using it blindly without accounting for its limitations; specifically for the following.

(i) A linear combination of bulge and disc is inadequate to model galaxy structures such as a nuclear point source, bars, rings etc., whenever they are sufficiently strong. Adding analytic models for these components greatly increases the free parameters in the minimization making it more likely to converge to an incorrect local minimum. Automated procedures that attempt to fit all these components are unlikely to give reliable results. We have therefore deliberately not added the ability to fit additional components to PyMorph. *GALFIT* does provide for modelling these features, but one needs to run it carefully on individual galaxies. In the rest-frame near-infrared, components like star-forming knots are quite weak. In addition, for distant galaxies, these small-scale features will be blended with the large-scale bulge and disc. In such cases, a linear combination of bulge and disc will likely be a robust model of the galaxy structure, although its physical interpretation is more complicated.

(ii) Certain minimization algorithms are more prone to converge to local minima (e.g. Levenberg–Marquardt used by *GALFIT*) than others (e.g. Metropolis algorithm used by *gim2d*). In practice, Häussler et al. (2007) have shown that *GALFIT* works better than *gim2d* in many situations. Users need to be aware of the capabilities and limitations of the algorithm and specific implementation being used.

(iii) Häussler et al. (2007) have pointed out that the SExtractor sky determination tends to overestimate the background. Incorrect background determination can affect parameter estimation, especially those of the bulge.

(iv) If one is fitting a pure disc galaxy, it often gets incorrectly fit by a Sérsic function with $n = 1$. This results in $B/T \sim 1$, which is clearly incorrect.

In order to assist the user in determining whether a particular galaxy has been correctly fit, *PyMorph* provides a diagnostic plot (see sample in Fig. 3). We recommend the following procedure to test for the quality of the fit, which users may adapt to their requirements.
(i) Check whether the FIT parameter in the output catalogue is unset. If it is unset it means that the reduced $\chi^2$ is larger than that the user specified in the config.py or the fitted centre of at least one component is incorrect.

(ii) Check for large residuals near the centre of the residual image in the diagnostic plot, which may be caused by a wrong PSF.

(iii) Check whether the difference histogram is centred at zero and well matched to the best-fitting Gaussian. If not, the residual image is not purely composed of noise.

(iv) Check whether the 1D profiles of original galaxy and the model galaxy match.

Through experience, the user will be able to rapidly identify problematic fits. Some of the quality checks above can be automated via scripts that use the information contained in the ASCII output files (result.csv) produced by PyMorph. Galaxies that are poorly fit may be handled using PyMorph in repeat mode (see Section 4).

### 5.2 Compare extracted CASGM parameters with published values

We have used a well-studied sample of nearby galaxies (Frei et al. 1996) with publicly available data to test the robustness of the CASGM parameters. We compare our estimated values with published values for these galaxies by Conselice (2003) and Lotz et al. (2004). This gives an idea of the robustness of our automated procedure. Figs 7 and 8 show the result of this comparison. We calculated the dispersion between our values and the published values. We found that the average deviation for concentration, asymmetry and clumpiness from that of Conselice (2003) are $-0.11 \pm 0.14$, $0.0 \pm 0.036$ and $0.06 \pm 0.09$, respectively. The average dispersion of our estimated values for Gini coefficient and second-order moment with that of Lotz et al. (2004) are $0.0 \pm 0.035$ and $0.0 \pm 0.16$. It will be interesting to compare the CAS values of Conselice (2003) with those Lotz et al. (2004) to show that similar dispersion was seen in previous comparisons. The dispersion between the CAS parameters reported in those papers are $0.08 \pm 0.16$, $-0.04 \pm 0.0445$ and $0.01 \pm 0.08$ for $C$, $A$ and $S$, respectively.

The small systematic offset of our concentration measurement from that of Conselice (2003) (see left-hand panel of Fig. 7) is due to the slight error in measuring the background value. This error will propagate to the measurement of $r_{20}$ and $r_{80}$ values. This effect is stronger in the case of galaxies with high concentration as they will have smaller $r_{20}$ and the slight uncertainty in $r_{20}$ leads to some variation in concentration index. It should be noted that this offset, though real, is small and within the error in many cases.

### 5.3 Simulating two-dimensional galaxy light profiles

To test the robustness of the structural parameters given by PyMorph we have run the code on simulated galaxy light profiles. In this section, we describe the simulation and then discuss the results. We
simulate surface brightness profiles of galaxies as a linear combination of a Sérsic and exponential functions. The steps involved in the simulation are the following.

1. Set the values of the parameters involved in the Sérsic and exponential functions. The range of these parameters used for simulation are $18 < m_b < 25$, $1 < r_e < 6$ kpc, $1 < r_d < 10$ kpc, $0.4 < e_b < 0.9$, $0.2 < e_d < 0.9$, where $m_b$, $r_e$, $e_b$ are the apparent magnitude, scale radius and axial ratio of bulge component of the galaxy, and $r_d$ and $e_d$ are the scale radius and axial ratio of the disc component. The range of Sérsic index used is $1 < n < 6.0$. These parameters are distributed uniformly along their respective ranges.

2. The Sérsic function is steeper towards the centre for large values of Sérsic index. Therefore, it is important to treat this cusp differently to generate exact surface brightness in the central region. We do this by oversampling the Sérsic function at the centre region. We oversample the central $5 \times 5$ pixels by a factor of 10. At the central pixel, we oversample the function 30 times while conserving the flux. For exponential function, the oversampling is done with a factor of 10.

3. We simulated 1000 objects as described in the previous step and inserted them into a $6000 \times 6000$ array. The position of these galaxy profiles in the large array is distributed randomly. This process is intended to simulate the original observation.

4. We then convolved the model image by the PSF. We have extracted a stellar image from an Advanced Camera for Surveys (ACS) observation for this purpose.

5. To simulate noise, we have generated a background image which has a typical standard deviation of the original observations of Hubble Space Telescope (HST) ACS/Wide-Field Planetary Camera 2 (WFPC2). The background values are distributed according to the Poisson distribution. Along with the background image we propagate the statistical error of the object counts determined from model image to create the noise image.

6. The model image and the background images are added to get the final simulated images and these images are used for further analysis.

5.4 Regression results for simulated galaxies

We have used PyMorph to extract parameters from the simulated images. The regression test results are shown in Fig. 9. We have calculated the mean magnitude per arcsec$^2$ within the half light radius of the galaxy, which is given by the SExtractor FLUX_RADIUS parameter. We found that for most of the cases the extracted parameters are within a fractional error of 50 per cent for a mean surface brightness <23 arcsec$^2$ (Fig. 10). It is found that for ~75 per cent objects the recovered parameters are within 20 per cent of the input value. Also for 90 per cent cases the recovered values are within 50 per cent of the input value. In Fig. 11 we show the fraction of recovered $B/T$ within different confidence levels. From that figure it is evident that more than 90 per cent of the galaxies are well within 50 per cent of the input value.

In Fig. 9 it can be seen that the bulge parameters are underestimated for some cases. We found that this is largely due to the overestimation of sky value by SExtractor. Because of this, if we fix the background value at the SExtractor value while fitting, we obtain incorrect bulge parameters. The result can be improved by leaving the background free (as we have done in our tests), but only a better algorithm to determine the sky can get rid of this problem completely.

![Figure 9: Input and recovered parameter values of galaxies at z = 0.8 where we have converted the physical parameters of galaxies such as scalelengths to pixel units using standard cosmology by assuming that the galaxies are at z = 0.8. The dark grey represents the region in which the fractional error is 20 per cent and light grey represents the regions of 50 per cent fractional error. The filled circles are for galaxies with magnitude <23.0 and open circles are for magnitude >23.0.](https://academic.oup.com/mnras/article-abstract/409/4/1379/984583)
5.5 Sensitivity to SExtractor input parameters

While running PyMorph, the user has some flexibility in choosing input parameters to SExtractor. It is important to test whether changes in SExtractor input parameters affect the final results, when processing real data. As a simple test, we used SDSS images of 160 galaxies in the i band randomly selected (from within four morphological classes in equal numbers) from the catalogue of ~14,000 visually classified galaxies from Nair & Abraham (2010). Our sample of 160 galaxies includes nearly equal number of all the morphological types (ellipticals, lenticulars, early-type spirals, late-type spirals). Our galaxies were selected to exclude those with bars/rings or any morphological components, other than bulge and disc.

The input parameters that are likely to change galaxy structural parameters significantly are those related to the detection threshold and background estimation. Therefore, we checked whether the final output of GALFIT changes significantly as these parameters of SExtractor are changed. We experimented with a detection threshold varying between 0.5 and 2.0. We checked whether the output varies if one uses GLOBAL background instead of LOCAL. We also varied the size of the background square used in SExtractor (64 and 128 pixels wide). In all these tests, there was no systematic deviation in extracted parameters, and an overwhelming fraction of galaxies were consistently fit.

6 Parallel PyMorph (PPyMorph)

When one thinks of the amount of data available from large astronomical surveys today and volumes that will be obtained with upcoming surveys, the need for parallelization of astronomical software, wherever feasible, emerges naturally. For the estimation of structural parameters, PyMorph needs significant computational time when operating on large samples. We, therefore, implemented PyMorph in the parallel mode to make use of large number of CPUs and process significant amount of data in a short time. The architecture of PPyMorph is simple. It uses the single program, multiple data technique. In this technique, we send different galaxy data to different processors in a cluster to achieve coarse parallelization. Each processor runs PyMorph on these data, and finally, all the results are collected together. We use the Python PyXPAR module extensively in PPyMorph.
Figure 12. The architecture of Parallel PyMorph. NP and NJ are the number of processors (SLAVES) and number of jobs (number of galaxies). Nth processor is the first available SLAVE.

Fig. 12 shows the architecture of parallel PyMorph. Here the user has the freedom to give input images in a variety of ways. It is possible to give a large frame(s) which contains several objects or cut-outs of objects. In all the cases PyMorph assigns one processor as the MASTER and that creates cut-outs of the galaxies. These are then sent, one by one, to an available processor in the cluster which is called a SLAVE. The SLAVE calls PyMorph to run on this cut-out image in galcut mode. While the SLAVE is working on the given cut-out, the MASTER searches for an unoccupied SLAVE and assigns another galaxy to it. This continues until all the available SLAVES are engaged. Then MASTER reads cut-out of additional galaxies in the list and waits, until one of the SLAVES finishes processing the galaxy assigned to it. When it finds a free SLAVE it fires the next job to that particular SLAVE. This process continues until the MASTER has no more galaxies left to fit. At this stage, the MASTER starts compilation of all the results by the SLAVES and creates final outputs (plots, html, csv etc.) for all galaxies.

In the non-parallel version, the pipeline takes ~100 s to generate all the structural parameters for a cut-out of size 240 × 240 on a computer with an Intel Core2 Duo CPU at 1.5 GHz with 2 GB RAM. In the parallel version, as the number of processors increases 10-fold, the required time decreases ~sixfold.

7 SUMMARY

We have presented a new software pipeline, PyMorph, to determine the structural parameters of galaxies in an automated way. We have described the methods implemented in the program. In the best cases, PyMorph uses a relatively small number of user-specified parameters, as compared to traditional fitting procedures. It makes extensive use of SEXTRACTOR and GALFIT. PyMorph tries to obtain a global minimum from GALFIT through clever use of the input parameters. We have tested the program for simulated data and compared our results with earlier published results. To increase processing speed, we have developed a parallel form of the pipeline.

Although PyMorph currently employs the popular GALFIT software as the minimization engine, it is flexible enough to allow the user to replace GALFIT with some other galaxy structural decomposition software, by modifying PyMorph.

The application of PyMorph ranges from individual images to large surveys. We have ourselves used the PyMorph pipeline for a study of galaxy morphology in clusters at moderate redshift (Vikram et al. 2010). Since it is implemented in PYTHON PyMorph is largely operating system independent. Also the implementation in PYTHON makes the code reusable. PyMorph makes it possible for astronomers to get structural parameters of a large number of galaxies in a short time. Given the complexity of the PyMorph package, we believe that some users will prefer to use a web enabled interface to PyMorph to obtain structural parameters for their galaxy images, without having to install the full PyMorph package. We are in the process of designing a virtual observatory compatible web interface to PyMorph in collaboration with VO-India.

A user manual of PyMorph is available at https://www.iucaa.ernet.in/~vinuv/UsersManual with detailed discussions on the input and output parameters. PyMorph source code is available on request.

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