OPF for large scale power system using ant lion optimization: a case study of the Algerian electrical network

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ABSTRACT

This paper presents a study of the optimal power flow (OPF) for a large scale power system. A metaheuristic search method based on the Ant Lion Optimizer (ALO) algorithm is presented and has been confirmed in the real and larger scale Algerian 114-bus system for the OPF problem with and without static VAR compensator (SVC) devices. To get the highest impact of SVC devices in terms of improving the voltage profile, minimize the total generation cost and reduction of active power losses, the ALO algorithm was applied to determine the optimal allocation of SVC devices. The results obtained by the ALO method were compared with other methods in the literature such as DE, GA-ED-PS, QP, and MOALO, to see the efficiency of the proposed method. The proposed method has been tested on the Algerian 114-bus system with objective functions is the minimization of total fuel cost (TGC) with two different vectors of variables control.

Keywords:
Ant lion optimizer (ALO)
Optimal power flow (OPF)
Static VAR compensator (SVC)
Total generation cost (TGC)

1. INTRODUCTION

Today's power industry needs the development of more complex nonlinear power system models and optimization techniques to solve them; these are called the optimal power flow problem (OPF) techniques. OPF is one of the most important tools for inefficient planning and controlling the operation of power systems. It was first introduced by [1]. The OPF procedure consists in choosing the optimal values of the control variables of an electrical system to optimize an objective function while satisfying the constraints of equality and inequality of the system [2]. Several objective functions related to the electrical system can be optimized, such as: minimize total generation cost (fuel cost, wind energy, cost of flexible transmission system (FACTS) cost, etc.), transmission losses, voltage deviation, voltage stability index, toxic gas emission, system safety, etc. [3-5]. The OPF problem can be considered as a large problem of nonlinear optimization with constraints. The optimization problem solved by several developed mathematical techniques, these techniques may be classified into two groups; conventional methods and recent intelligence methods (evolutionary or metaheuristic methods). Recently, several evolutionary or metaheuristic optimization methods have been proposed to get the best solution to the OPF problem.

Metaheuristic algorithms (MAs) mark a great revolution in the field of optimization, allow finding one or more solutions to complex optimization problems [6]. According to [7], the MAs can be regrouped into four main categories: evolution-based methods, physics-based methods, human-based methods, and swarm-based methods. Several metaheuristic algorithms are implemented in electrical power system for

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solving the optimal power flow problem with different objective functions such as moth flame optimizer (MFO) [4], enriched brain storm optimization (EBSO) [8], moth swarm algorithm (MSA) [9], particle swarm optimization (PSO) [10], cat swarm optimization (CSO) [11], chaotic whale optimization algorithm (IABC) [12], improved strength Pareto evolutionary algorithm (IEA) [13], symbiotic organisms search algorithm (SOSA) [14], stud krill herd algorithm (SKH) [15], modified Grey wolf optimizer (MGWO) [16], differential search algorithm (DSA) [17] and integrated algorithm (IA) [18].

This paper presents one of the newest flexibility and efficient optimization metaheuristic method, called ant lion optimization (ALO). Recently, many researchers are interested in this method for solving the optimization problem, as in [19-20]. In this study, the proposed method has been applied for solving the OPF problem for large scale power systems which is the Algerian 114-bus power system. Two different cases are considered, with and without the presence of SVC devices. The objective function used in this paper is minimizing the total fuel cost (TFC).

2. MODELING OF SVC DEVICE

The static VAR compensator SVC is modeled by shunt variable admittance. Since the power loss of the SVC device is assumed negligible, so the admittance is assumed purely imaginary as follow:

\[ y_{SVC} = jb_{SVC} \]  

(1)

The susceptance \( b_{SVC} \) can be capacitive or inductive to respectively provide or absorb the reactive power \( Q_{SVC} \). The placement of SVC devices in this study is installed in the power system as a PV bus with the real power generation equal to 0 MW. The reactive power \( Q_{SVC} \) absorbed by the SVC device and also injected into node \( i \) is given by (2):

\[ Q_{SVC} = -V_i^2 b_{SVC} \]  

(2)

3. OPTIMAL POWER FLOW (OPF) PROBLEM FORMULATION

3.1. Formulation problem

The solution of the OPF problem aims to minimize or maximize an objective function for getting an optimal adjustment of control variables in the power system by satisfying both constraints, equality and inequality constraints. Generally, the optimization problem can be represented mathematically as follows:

\[ \text{Min } F(x, u) \]  

(3)

Subjected to \( g(x, u) = 0 \)  

(4)

\[ h(x, u) \leq 0 \]  

(5)

where: \( F \) represents the objective function, \( x \) represents the vector of the state variables and \( u \) represents the vector of the control variables.

3.2. Objective function

The objective function in this study is the quadratic equation of generation fuel cost of each available conventional generator subject to operating constraints and formulated as follows:

\[ C_i(P_{Gi}) = \sum_{i=1}^{NG} a_i + b_i P_{Gi} + c_i P_{Gi}^2 \]  

(6)

where \( C_i(P_{Gi}) \) is the fuel cost of the \( i \)th generator, \( P_{Gi} \) is the active power generated by the thermal generators, \( a_i, b_i \) and \( c_i \) are the cost coefficients of \( i \)th generator.
Equality constraints:
The equality constraints represent the flow equations of the balanced powers as follows:

\[ P_{gi} - P_{d_i} = V_i \sum_{j=1}^{N} V_j \left( g_{ij} \cos \delta_j + z_{ij} \sin \delta_j \right) \]  

\[ Q_{gi} - Q_{d_i} = V_i \sum_{j=1}^{N} V_j \left( g_{ij} \sin \delta_j + z_{ij} \cos \delta_j \right) \]  

Inequality constraints:
The equality constraints represent the limits of variable control and state control of the power system and can be given as follows:

\[
\begin{align*}
P_{Gi}^{\text{min}} & \leq P_{Gi} \leq P_{Gi}^{\text{max}} \\
Q_{Gi}^{\text{min}} & \leq Q_{Gi} \leq Q_{Gi}^{\text{max}} \\
V_{Gi}^{\text{min}} & \leq V_{Gi} \leq V_{Gi}^{\text{max}} \\
T_{NTi}^{\text{min}} & \leq T_{NTi} \leq T_{NTi}^{\text{max}} \\
Q_{SVCi}^{\text{min}} & \leq Q_{SVCi} \leq Q_{SVCi}^{\text{max}} \\
|S_{Li}| & \leq S_{Li}^{\text{max}}
\end{align*}
\]

(9)

The vectors of control variables \( u_1 \) and \( u_2 \) are respectively the cases without and with the presence of SVC devices on the power system, and can be described as follows:

\[ u_1 = [P_{G2} \ldots P_{GNG}] \]  

\[ u_2 = [P_{G2} \ldots P_{GNG}, V_{G1} \ldots V_{GNG}, Q_{SVC1} \ldots Q_{NSVC}] \]  

(10) (11)

Where: \( P_{Gi} \) are the active powers generated, \( V_L \) is the generator voltage and \( Q_{SVC} \) is the reactive power injected by the SVC device.

4. THE ANT LION OPTIMIZATION (ALO) ALGORITHM

The ant lion optimizer (ALO) is considered as the most recent nature-inspired proposed by [21]. The modeling of the ALO algorithm based on the hunting mechanism of ant lions in nature. The main objective of the ALO algorithm is to solve any optimization problems of constrained engineering, it can get an optimal solution for minimizing the objective function by satisfying various constraints. In the ALO mechanism, it can be hunting the prey (ant) through five main steps as follow; random walk of ants, building traps, trapping in antlions traps, sliding prey toward antlion and final step are catching preys and rebuilding traps for a new step of hunting.

The ALO method mimics the hunting behavior of ant lions, the expression mathematically of the random walks of ants to detect the location of food is describes as follow:

\[ X(t) = \left[ 0, \text{cumsu}(2r(t_1) - 1), \text{cumsu}(2r(t_2) - 1), \ldots, \text{cumsu}(2r(t_n) - 1) \right] \]  

(12)

where \( X \) denotes the random walks of ants, \( \text{cumsu} \) is the cumulative sum, \( t \) is the step of random walk, \( n \) is the maximum iterations and \( r(t) \) show the stochastic function and given as follows:

\[ r(t) = \begin{cases} 
1 & \text{if } \text{rand} > 0.5 \\
0 & \text{if } \text{rand} < 0.5 
\end{cases} \]  

(13)
where $\text{rand}$ represents a randomly number uniformly distributed in the range of $[0,1]$.

The Details of different steps describe the relationship between predators and preys in the ALO method are explained as follow:

4.1. Random walk of ants

In every step of optimization in the ALO algorithm, ants move randomly inside the boundaries of the search space based on the (14), the random walks of ants are normalized by using the following:

$$X'_i = \frac{(X'_i - a_i) * (b'_i - c'_i)}{(b_i - a_i)} + c'_i$$ (14)

where the $a_i; b_i$ denotes the minimum and maximum of random walk respectively. $c'_i$ and $d'_i$ are indicated the minimum and maximum of $ith$ variables at $tth$ iteration.

4.2. Trapping in antlions traps

The random walks of ants are influenced by antlions traps and are modeled as follows:

$$c'_i = \text{Antlion}'_j + c'$$ (15)

$$d'_i = \text{Antlion}'_j + d'$$ (16)

4.3. Building traps

In this work, the ALO algorithm is required to use a roulette wheel selection operator for selecting the better antlions based on their higher fitness, forgive a high chance for catching ants.

4.4. Sliding ants toward antlion

When the ants move toward near the center of the pit. However, once antlions realize that an ant is in the trap, they shoot sands outwards the center of the pit. To model this mechanism mathematically, the radius of the ant’s random walk is decreased correspondingly using (17) and (18):

$$c' = \frac{c'}{I}$$ (17)

$$d' = \frac{d'}{I}$$ (18)

4.5. Catching preys and rebuilding the traps

The final step of hunting is when the prey reaches into the bottom of the antlion pit and is caught in the antlion’s jaw. After this stage, the antlion pulls the prey inside the sand and consumes its body. Then the antlion updates its new position to the latest position of the ant, to enhance its chance of catching new prey. The equation which models the catching prey and rebuilds the pits is given as follows:

$$\text{Antlion}'_j = \text{Ant}'_t, \quad \text{if } f(\text{Ant}'_t) > f(\text{Antlion}'_j)$$ (19)

where $\text{Antlion}'_j, \text{Ant}'_t$ represents the position of the selected jth antlion and ith ant at iteration $t$.

4.6. Elitism

The elitism of an ant lion is determined by using the roulette wheel selection (RWs) at each step of optimization. The best antlion selected should be capable to affect the movements of all the ants at any iteration is saved as elite. The elitism mechanism for repositioning of a given ant described in the following equation:

$$\text{Ant}'_t = \frac{R'_A + R'_E}{2}$$ (20)
where $R_{At}^t$ is the random walk around the selected antlion using the roulette wheel at $t$ – $th$ iteration, $R_{Et}^t$ is the random walk around the elite antlion at $t$ – $th$ iteration.

5. RESULTS AND ANALYSIS

In order to show the performance and efficiency of the proposed algorithm ALO to solve optimization in the larger system dimensions, the OPF has been performed on the Algerian 114–bus system. This system network involves 15 generators, 175 lines, 16 tap changer transformers are located from line 160 to line 175 and 99 load bus of total demand are 3,727 MW and 2070 MVar. The economic and technical parameters of 15 generators in the of the Algerian 114–bus power system in Ref. [22]. In this study, the proposed algorithm has been applied on the system under two different simulation cases that are considered, with and without static VAR compensator (SVC) devices. In the two simulation cases, 30 independent runs were executed for establishing the superiority of the ALO method with the population size equal to NP = 40 and the maximal iterations are 200. The flowchart of the implementation of the proposed algorithm for solving the OPF problem that minimizes the total generation cost is shown in Figure 1.

5.1. OPF for Algerian electrical network system without SVC devices

In this first case, we perform simulations on the Algerian 114–bus system without the SVC device. The objective function used is minimizing the fuel cost of 15 thermal generators and the vector of control variables contains the active powers generated as shown in (10). The optimization results obtained by the ALO algorithm compared with the grey wolf optimizer (GWO) and other optimization methods in the literature are tabulated in Table 1. The corresponding convergence of the proposed algorithm and GWO algorithm is shown in Figure 3.
The optimal values of control variables, total generation cost, and active power losses are summarized in Table 2. Over 30 independent trial runs were executed in this case as shown in Figure 2. From these results obtained, the best value of total generation cost and active power losses by the proposed method are $19141.7714 \$/h and 76.3446 MW respectively, these values are better than the results obtained by different algorithms previously reported in Table 1. The Figure 3, allows us to note, in the first place, that the method ALO converges towards the global optimum at the iteration 100 while the convergence of the GWO method is reached at the iteration 180. So, the results obtained showed the proposed method ALO superior and robust compared to the GWO method in terms of getting the best solution for solving the OPF problem.

| Variables | limits | ALO  | GWO  | DE [22] | GA-ED-PS [23] | QP [24] | MOALO [25] |
|-----------|--------|------|------|---------|---------------|---------|------------|
| $P_{G1}(MW)$ | 135 1350 | 438.2927 | 449.2373 | 462.3908 | 455.9113 | 449.559 | 458.0600 |
| $P_{G2}(MW)$ | 135 1350 | 452.1957 | 455.3286 | 459.5589 | 455.9219 | 449.559 | 451.1905 |
| $P_{G11}(MW)$ | 10 100 | 99 9064 | 99 9064 | 100 0000 | 100 0000 | 100 0000 | 74 91904 |
| $P_{G12}(MW)$ | 30 300 | 199 3340 | 193 9445 | 192 5196 | 194 3179 | 195 368 | 212 0149 |
| $P_{G13}(MW)$ | 135 1350 | 444.4851 | 453.0225 | 453.0142 | 448.7254 | 449.559 | 436 8922 |
| $P_{G14}(MW)$ | 34.5 345 | 204.8873 | 193.5834 | 196 6569 | 196 0150 | 195 368 | 236 6123 |
| $P_{G22}(MW)$ | 34.5 345 | 207.6710 | 191.9811 | 189 0239 | 190 8388 | 195 368 | 197 7529 |
| $P_{G23}(MW)$ | 34.5 345 | 192.2261 | 185.6850 | 193.9372 | 197.8609 | 195 368 | 246 6429 |
| $P_{G25}(MW)$ | 34.5 345 | 194.8395 | 193.3146 | 192 1215 | 193 7835 | 195 368 | 171 7571 |
| $P_{G3}(MW)$ | 30 300 | 191.3274 | 189 5693 | 188.1283 | 190 9545 | 195 368 | 163 4842 |
| $P_{G6}(MW)$ | 30 300 | 184.6229 | 196 7435 | 189.0847 | 191 9255 | 195 368 | 214 0323 |
| $P_{G10}(MW)$ | 60 600 | 600 0000 | 600 0000 | 599.9752 | 600 0000 | 600 0000 | 599 9999 |
| $P_{G11}(MW)$ | 20 200 | 200.0000 | 200.0000 | 199.9703 | 200.0000 | 200.0000 | 199 9999 |
| $P_{G12}(MW)$ | 10 100 | 99.9996 | 100.0000 | 99.9909 | 100.0000 | 100.0000 | 67 19996 |
| $P_{G13}(MW)$ | 10 100 | 93.5897 | 99.8715 | 99.9415 | 100.0000 | 100.0000 | 81.96231 |

Active power loss (MW) | 76.3446 | 75.1879 | 89.2570 | 89.2570 | - |

The optimal values of control variables, total generation cost, and active power losses are summarized in Table 2. Over 30 independent trial runs were executed in this case as shown in Figure 2. From these results obtained, the best value of total generation cost and active power losses by the proposed method are $19141.7714 \$/h and 76.3446 MW respectively, these values are better than the results obtained by different algorithms previously reported in Table 1. The Figure 3, allows us to note, in the first place, that the method ALO converges towards the global optimum at the iteration 100 while the convergence of the GWO method is reached at the iteration 180. So, the results obtained showed the proposed method ALO superior and robust compared to the GWO method in terms of getting the best solution for solving the OPF problem.
5.2. OPF for Algerian electrical network system with SVC devices

In this case, the SVC devices are implemented in the Algerian 114-bus system to improve the voltage profile and reduce the TFC. The vector of control variables, in this case, contains the active powers generated, the generator voltage, and the reactive power injected by the SVC devices as shown in (11). The first optimal placement of the SVC device in the Algerian 114-bus system at bus N°89 (Souk Ahras), and bus N°68 (Sedjerara). The optimization results are given in Table 2.

Table 2. Optimization results obtained by ALO with different optimal placement of SVC

| Variables | Limits | Without SVC | SVC Bus N°89 | SVC Bus N°89 | SVC Bus N°68 & 89 |
|-----------|--------|-------------|--------------|--------------|-------------------|
| P_G1 (MW) | Min 135 | Max 150     | 439.6459     | 428.7504     | 422.0728          | 432.5625          |
| P_G2 (MW) | Min 135 | Max 150     | 448.1696     | 435.1449     | 426.7332          | 439.0722          |
| P_G1 (MW) | Min 10  | Max 100     | 82.0231      | 93.1780      | 100.0000          | 100.0000          |
| P_G2 (MW) | Min 30  | Max 300     | 171.8617     | 223.7201     | 235.9225          | 229.0151          |
| P_G1 (MW) | Min 135 | Max 150     | 443.1784     | 437.5715     | 420.1050          | 441.9554          |
| P_G2 (MW) | Min 34.5| Max 345     | 209.4855     | 196.8190     | 184.4021          | 162.6831          |
| P_G2 (MW) | Min 34.5| Max 345     | 186.9316     | 187.4384     | 167.9495          | 218.4372          |
| P_G2 (MW) | Min 34.5| Max 345     | 216.0484     | 224.8141     | 221.2963          | 198.0932          |
| P_G2 (MW) | Min 34.5| Max 345     | 232.0432     | 211.1695     | 198.3792          | 180.6525          |
| P_G2 (MW) | Min 30  | Max 300     | 192.5640     | 185.8489     | 224.2547          | 221.0994          |
| P_G2 (MW) | Min 30  | Max 300     | 165.8376     | 174.1723     | 186.9096          | 161.7763          |
| P_G2 (MW) | Min 60  | Max 600     | 599.9998     | 600.0000     | 600.0000          | 600.0000          |
| P_G2 (MW) | Min 20  | Max 200     | 199.9999     | 200.0000     | 200.0000          | 199.9999          |
| P_G2 (MW) | Min 10  | Max 100     | 99.9999      | 94.2300      | 99.2689           | 99.9999           |
| P_G2 (MW) | Min 10  | Max 100     | 99.9997      | 94.3467      | 99.9996           | 100.0000          |
| Q_v1 (Mvar) | Min 1.14 | Max 90 | 0.9023     | 0.9273        | 0.9393            | 20.9159           |
| Q_v89 (Mvar) | Min -45 | Max 45 | 20.9076     | -             | 33.4490           | 33.3790           |
| Total generation cost ($/h) | Min 19061.4915 | Max 19042.7382 | 19023.2724 | 18999.6809 |
| Active power loss (MW) | Min 60.7884 | Max 60.9076 | 60.0237 | 60.2935 | 58.3467 |

Table 2 shows the results of TFC and real power losses obtained by using the proposed algorithm in the case without and with SVC devices, separately or multiple in buses N°68 and N°89. From these results obtained, it can be observed that the presence of SVC devices in all cases improved considerably the TGC and active power loss. The convergence curve of the proposed algorithm is shown in Figure 4. From this figure, we notice that the algorithm ALO converges towards the global optimum at the iteration 100 for all cases study when the SVC devices installed.

Figure 4. Convergence plot of ALO methods in the Algerian 114 bus power system

On the other hand, SVC devices have managed to improve the voltage profile as shown in Figure 5, from this figure, it can be noted that the case without the presence of SVC, the two circles in this figure determine the two areas that have critical load bus voltage in Algeria 114-bus system. So, when the SVC
devices were installed at busses 68 and 89 separately or multiple, the voltage values of this optimal emplacement were increased to 1 p.u as shown in Figure 5, respectively. Furthermore, this increment in the voltage values in the optimal placement of SVC allows for improving the voltage at the critical load buses compared to the previous case (without the presence of SVC device).

Figure 5. The effect of SVC device on the voltage profile in the Algerian 114-bus power system

6. CONCLUSION

In this paper, we have validated the new metaheuristic technique, called, Ant Lion Optimizer (ALO) for real and large scale Algerian 114-bus power system to solve optimal power flow (OPF) problem. The ALO algorithm was successfully applied to solve the OPF problem with and without SVC devices. From the results obtained in the case without the SVC device, the proposed algorithm has been the best result compared with the method developed by us, called, grey wolf optimization and other methods in the literature defined in this paper, like DE, GA-ED-PS, and OP. In the case with the presence of SVC devices, the ALO algorithm was used to identify the optimal sizing and placement of SVC devices in the Algerian 114-bus system based on the location of the lowest voltage load buses in the power system. The optimization results achieved by using the ALO algorithm with presence the of SVC devices given the best results to minimize the total fuel cost, reduce the active power losses and improving the voltage profile based on the optimal placement and sizing of SVC devices. Based on the results of both case studies in this paper, it can be concluded that the ALO algorithm is capable of solving the OPF problem for a large scale power system with and without the presence of SVC devices.

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