Common exotic decays of top partners

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ABSTRACT: Many standard model extensions that address the hierarchy problem contain Dirac-fermion partners of the top quark, which are typically expected around the TeV scale. Searches for these vector-like quarks mostly focus on their decay into electroweak gauge bosons and Higgs plus a standard model quark. In this article, backed by models of composite Higgs, we propose a set of simplified scenarios, with effective Lagrangians and benchmarks, that include more exotic decay channels, which modify the search strategies and affect the bounds. Analysing several classes of underlying models, we show that exotic decays are the norm and commonly appear with significant rates. All these models contain light new scalars that couple to top partners with charge 5/3, 2/3, and −1/3.

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1 Introduction

Heavy vector-like quarks (VLQs in the following) are extensively searched for at the LHC due to the important role they play in many models beyond the standard model (BSM). The qualification ‘vector-like’ refers to the fact that, contrary to fermions in the standard model (SM), both VLQ chiralities share the same quantum numbers under the SM gauge symmetries. Among the models that predict VLQs, models of composite Higgs have a special stand due to the crucial role the VLQs play for the top quark and Higgs physics. The Higgs is assumed to arise as a composite scalar of a confining and condensing underlying interaction, and its lightness compared to the condensation scale can be accounted for by the Higgs being a pseudo-Nambu-Goldstone boson (pNGB) \[1, 2\]. VLQs materialise as composite fermions, which generate masses for the top (and, eventually, lighter fermions) via the mechanism of partial compositeness (PC) [3], i.e. via linear mixing terms between the elementary and the composite fermions. It is also widely accepted that light VLQs (aka top partners) are needed in order to stabilise the loop-induced Higgs potential and keep the Higgs mass light (see, for instance, refs. [4, 5]). We stress that this conclusion is based on the strong assumption of an enhanced calculability present in the effective theory below the condensation scale [6, 7]. This is, however, not always the case for strongly interacting and confining theories (as QCD teaches us). Furthermore, the stabilisation of the Higgs potential can also be achieved without top partners, for instance by tuning a mass term for the underlying fermions [8, 9]. VLQs also play a useful role in other models, like supersymmetry [10–12], and their phenomenology can be studied in effective models, independently of the theoretical framework they come from (see, for instance, refs. [13–18]).
In this article, we use the framework of partial compositeness and a composite pNGB Higgs as a guide for characterising the phenomenology of VLQs. This has already been the guiding principle behind the current experimental VLQ searches. However, the phenomenological expectations were strongly based on the most minimal model, where the Higgs boson is the only light pNGB in the theory 19. The two main assumptions, which have been used for most searches, are first, that the VLQ only decays to a standard boson (W, Z and the Higgs h) plus a SM quark, and second, that the quarks belong to the third generation, i.e. only top or bottom quarks. We will show that, in models that enjoy a simple underlying description in terms of a confining gauge symmetry, the first assumption is not well justified. In fact, generically new decay channels are present that often dominate over the standard ones. The main underlying reason is that the most minimal symmetry breaking pattern SO(5) → SO(4) is not realised in any known simple underlying model, and thus additional light pNGBs are present in the spectrum. This is true both in models where only fermions are present, as described in refs. 20–23, and in models with fermion-scalar bound states 24, 25.

Analysing the classes of models in the literature, we identify 4 types of situations that can strongly affect top partner decays, as summarised below:

1. **Singlet pseudo-scalar**, \(T \rightarrow t a\) and \(B \rightarrow b a\). The presence of a light CP-odd pNGB associated to a non-anomalous U(1) global symmetry is ubiquitous to models of PC with a gauge-fermion underlying description 26–30. We show that the light pseudo-scalar \(a\) always couples to the top partners. Thus, a charge 2/3 VLQ \(T\) and a charge −1/3 VLQ \(B\) also decay to \(a\) and a SM quark, as long as the pNGB \(a\) is lighter than the VLQ. While the presence of \(a\) adds VLQ decay channels, the pair and single production rates of the VLQs are barely modified.

2. **Exclusive pNGB**, \(\tilde{T} \rightarrow t \eta\). The extended pNGB cosets may also contain additional scalars that couple exclusively with one specific top partner, \(\tilde{T}\). This is the case for a CP-odd singlet \(\eta\) present in the SU(4)/Sp(4) ≃ SO(6)/SO(5) coset 31–33. The charge 2/3 top partner \(\tilde{T}\), which is part of a 5 of Sp(4) ≃ SO(5), does not decay to two SM particles but exclusively into \(t \eta\), and it cannot be singly- but only pair-produced at colliders.

3. **Coloured pNGB**, \(X_{5/3} \rightarrow \bar{b} \pi_6\). The presence of coloured fermions or scalars in the underlying theory yields potentially light coloured pNGBs. Their couplings to the VLQs imply additional decay channels beyond the standard ones. As an example, we consider a pNGB transforming as a sextet of QCD colour and with charge 4/3. This state is present in some underlying models 34, and it can couple to the exotic charge 5/3 top partner \(X_{5/3}\). Note that coloured pNGBs can also modify the production rates of the VLQs, especially if heavier than them 35.

4. **Charged pNGB**, \(X_{5/3} \rightarrow t \phi^+\). Some cosets, like SU(5)/SO(5) 23, also contain additional charged pNGBs which contribute to the decays of the top partners. These decay channels are usually present in addition to the standard ones.
A fifth possibility is that some top partners can decay into a stable (or long-lived) pNGB, which may be identified with a Dark Matter candidate: typically, this leads to exclusive decay modes, as shown in refs. [36–38]. Such decay modes are efficiently covered by searches focused on supersymmetric final states [39]. Thus, we do not consider this possibility here.

In section 2, we introduce simplified model descriptions and benchmark points for the scenarios listed above. We discuss how the standard searches for VLQs are affected by the new decay modes and which new experimentally promising signatures arise. Several additional decay modes for VLQs have already been considered in the literature, both for composite models [32, 40] and supersymmetric models [41] (see also ref. [42] for a more general table of allowed final states). Our approach differs, as we identify testable predictions which arise from models with a simple underlying description, where the new modes are predicted and not added by hand. To better substantiate this, in section 3, we present underlying models and model-parameters that predict the field content of the simplified models of section 2 as part of their (light) particle spectrum, and that yield the effective couplings used as benchmark points. Finally, we present our conclusions in section 4.

2 Simplified scenarios

2.1 Singlet pseudo-scalar, $T \to t \ a$ and $B \to b \ a$

As a first simplified scenario, we consider a model with a charge 2/3 top partner $T$ and a lighter pseudo-scalar $a$. Such a light pseudo-scalar $a$ is genuinely present in models of PC with a gauge-fermion underlying description [26–30], where it can be associated with the pNGB of a global U(1) symmetry. We parameterise the interactions of a VLQ with SM particles and the pseudo-scalar $a$ as

$$\mathcal{L}_T = \bar{T}(i\gamma_5 - M_T)T + \left(\kappa_{W,L}^T g \sqrt{2} \bar{T}W^+P_Lb + \kappa_{Z,L}^T g_{2c_W} \bar{T}ZP_Lt - \kappa_{h,L}^T M_T v \bar{T}hP_Lt + i\kappa_{a,L}^T \bar{T}aP_Lt + L \leftrightarrow R + h.c\right), \tag{2.1}$$

where $P_{L,R}$ are left- and right-handed projectors, and $T$ denotes the top partner mass eigenstate with mass $M_T$. The first three interaction terms dictate the partial widths of $T$ decays into $bW, tZ,$ and $th$ as often considered in VLQ models. In the above parametrisation, the coefficients $\kappa_{W/Z/h,L,R}^T$ are determined by the SU(2) charge and the mixing angles of the top partner with the elementary top. If only decays into SM particles are considered, the current bound is of order $M_T \gtrsim 1 \ TeV$ [43–49]. The last term in eq. (2.1) parameterises the coupling of $T$ to the pseudo-scalar $a$. This term does not significantly

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1 We follow the parametrisation of ref. [18] for the couplings to SM particles.

2 Bounds on $M_T$ from QCD produced $T$-pairs depend on the $T$ branching ratios (BRs) into $bW, tZ, th$. The strongest reported bound is for 100% BR $T \to bW$ ($M_T \gtrsim 1.3 \ TeV$) [43, 45], while bounds on 100% BR $T \to tZ$ or $T \to th$ are around 1 TeV. Bounds on $M_T$ from electroweak single-production [50–56] are even more model-dependent as the production cross section depends on additional BSM couplings.
affect the top-partner production, which occurs through QCD pair production, or through single-production dictated by the first three terms (cf. e.g. refs. \[18, 19\] for top partner single- and pair production rates). If \(M_T > m_a + m_t\), the last term in eq. (2.1) adds an additional decay channel of \(T \to t a\). Explicit expressions for the tree-level decay widths can be found in ref. \([57]\).

In analogy, as a second simplified model, we introduce the VLQ \(B\) with charge \(-\frac{1}{3}\), with the simplified Lagrangian

\[
\mathcal{L}_B = \overline{B} \left( i \gamma^\mu - M_B \right) B + \left( \kappa^B_{W,L} \frac{g}{\sqrt{2}} \overline{B} W^- P_L t + \kappa^B_{Z,L} \frac{g}{2c_W} \overline{B} Z^+ P_L b \right) - \kappa^B_{h,L} \frac{M_B}{v} \overline{B} h P_L b + i \kappa^B_{a,L} \overline{B} a P_L b + \text{L} \leftrightarrow \text{R} + \text{h.c.} \right).
\]

To illustrate the relevance of the new decay channels, we consider two benchmark models, “Bm1” and “Bm2”, arising from an underlying UV embedding of composite Higgs models with SU(4)/Sp(4) breaking, which are discussed more in detail in section 3. In figure 1 we show the BRs in the two benchmarks as a function of the \(a\) mass. Each scenario focuses on one VLQ, either \(T\) or \(B\). The two benchmark models are respectively characterised by the following couplings:

**Bm1:** \(M_T = 1\) TeV, \(\kappa^T_{Z,R} = -0.03\), \(\kappa^T_{h,R} = 0.06\), \(\kappa^T_{a,R} = -0.24\), \(\kappa^T_{a,L} = -0.07\);

**Bm2:** \(M_B = 1.38\) TeV, \(\kappa^B_{W,L} = 0.02\), \(\kappa^B_{W,R} = -0.08\), \(\kappa^B_{a,L} = -0.25\),

while the ones that are not reported are suppressed and thus negligible. The BRs of \(T \to t a\) and \(B \to b a\) are model dependent. However, the benchmarks we present in figure 1, which are fairly generic and not tuned to maximise the new channels, clearly show that, in fully realistic models, they can be sizeable and even comparable to the BRs into SM particles, which are considered in standard searches at the LHC.

To determine new possible final states that can occur from the \(T \to t a\) (or \(B \to b a\)) decay, we briefly review the properties of, and constraints on, the pseudo-scalar \(a\). The
interactions of the pseudo-scalar $a$ with SM particles can be parameterised as\footnote{We give the effective Lagrangian up to dimension 5 operators. Additional interactions can be generated at higher order. See ref.\cite{Abe:2018uqu} for couplings $h\alpha a$ and $hZ a$.}

\[
\mathcal{L}_a = \frac{1}{2} (\partial_\mu a)(\partial^\mu a) - \frac{1}{2} m_a^2 a^2 - \sum_f \frac{i C^q_a m_f}{f_a} a f^5 f + \frac{g^2 K^a_a}{16\pi^2 f_a} a G^{\mu\nu}_a G_{\mu\nu}^a + \frac{g^2 K^a_w}{8\pi^2 f_a} a W^+ \gamma W^- \mu\nu \\
+ \frac{e^2 K^a_\gamma}{16\pi^2 f_a} a A_{\mu\nu} A^{\mu\nu} + \frac{g^2 c^2_W K^a_\gamma}{16\pi^2 f_a} a Z_{\mu\nu} Z^{\mu\nu} + \frac{eg c_W K^a_\gamma}{8\pi^2 f_a} a A_{\mu\nu} Z^{\mu\nu} .
\] (2.4)

Note that we have written the couplings to the gauge bosons in the mass eigenstate basis because the mass of $a$ can well be around or below the electroweak (EW) scale, and we define $V_{\mu\nu} = \partial_\mu V_{\nu} - \partial_\nu V_{\mu}$ and $\bar{V}_{\mu\nu} = \epsilon_{\mu\nu\rho\sigma} V^{\rho\sigma}$. The couplings are, in general, independent, but relations among them may exist depending on the origin of the pseudo-scalar $a$. In underlying models where $a$ is associated to a U(1) symmetry \cite{Abe:2018uqu,Bertolini:2019zoy}, the couplings to gauge bosons can be determined in terms of two parameters: one coupling, $K^a_W$, to the SU(2) bosons and one, $K^a_B$, to hypercharge. Thus, we have the relations

\[
K^a_\gamma = K^a_W + K^a_B , \quad K^a_Z = K^a_W + K^a_B h_W^4 , \quad K^a_B = K^a_W - K^a_B h_W^4 ,
\] (2.5)

where $t_W = \tan(\theta_W)$ is the tangent of the Weinberg angle. The parameters $K^a_{W,B}$ are fully determined in terms of the underlying theory. On the other hand, the couplings to the fermions depend on the origin of the mass terms, i.e. the choice of top partners and the values of the mixing couplings (more details will be provided in section 3). For a given model and choice of the fermion couplings, the only other remaining parameters are the decay constant $f_a$, which controls the overall width and coupling strength, and the mass $m_a$, on which the BRs depend. The latter can be potentially very small, of the order of few GeV \cite{Abe:2018uqu}. As an example, the couplings resulting from the SU(4)/Sp(4) model discussed in section 3.2 are

\[
K^a_g = -1.6 , \quad K^a_W = 1.9 , \quad K^a_B = -2.3 , \quad C^a_{f\neq t} = 1.9 , \quad C^a_t = \begin{cases} 1.46 & \text{for Bm1} \\ 2.33 & \text{for Bm2} \end{cases} ,
\] (2.6)

where from the UV model, we also fix $f_a = 2.8$ TeV, and only leave the mass $m_a$ as a free parameter. They correspond to the underlying model M8, discussed in ref.\cite{Abe:2018uqu}. The BRs of $a$ for this parameter choice (for Bm1) are shown in figure 2 (left) as a function of $m_a$. The BRs do not depend on the decay constant $f_a$.

The pseudo-scalar $a$ can be directly produced at the LHC in gluon fusion.\footnote{Top-associated production (tta) is also possible — in particular for light $a$ \cite{Dreiner:2018gmy}. Furthermore, light $a$ can result from $h \rightarrow a a$ or $h \rightarrow Z a$ decays \cite{Dreiner:2018ajf}. For the benchmark models considered in section 3, these processes only yield weak bounds, however, as shown in ref.\cite{Abe:2018uqu}.} As the BRs of $a$ are determined as given in figure 2, bounds from ATLAS and CMS resonance searches in the channels $jj$ \cite{Aaboud:2017ldz,Aaboud:2017qkw,Aaboud:2018jag,Aaboud:2018npp}, $t\bar{t}$ \cite{Aaboud:2017zdy,Aad:2015kca,Aad:2019kps,Aad:2019zbu}, $b\bar{b}$ \cite{Aaboud:2017vjd}, $\tau^+\tau^-$ \cite{Aaboud:2017zyr,Aaboud:2018vrd,Aaboud:2018fyl,Aaboud:2018llz}, $\mu^+\mu^-$ \cite{Aad:2015mga}, $W^+W^-$ \cite{Aad:2015sba,Aad:2016pqn,Aad:2017flm,Aad:2017jac,Aad:2017zbn,Aaboud:2018wme,Aaboud:2018zau,Aaboud:2018zfp}, $ZZ$ \cite{Aad:2017jus,Aad:2018yci,Aad:2018wwe}, $Z\gamma$ \cite{Aad:2015vwa,Aad:2016fpa,Aad:2018aqb,Aad:2018ann,Aad:2018oid}, $\gamma\gamma$ \cite{Aad:2018oic,Aaboud:2018vfr,Aaboud:2018juw,Aad:2019xud,Aad:2019gfs,Aad:2019yuw,Aad:2019foo} can be translated into bounds on the decay constant $f_a$, which controls the direct production cross section \cite{Abe:2018uqu,Bertolini:2019zoy}. The right panel in figure 2 shows the resulting bounds on $f_a$ for the benchmarks Bm1 and Bm2 characterised

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Figure 2. Left: branching ratios of $a$ as a function of the mass $m_a$ in the benchmark model Bm1 characterised by the parameters in eq. (2.6). Right: experimental lower bounds on $f_a$ from ATLAS and CMS resonance searches on the benchmark models Bm1 (blue) and Bm2 (black) as compared to the underlying theory value (red).

by the couplings given in eq. (2.6). The red line corresponds to the estimated value of $f_a$ from the underlying model (see section 3.2). As it can be seen, this value is not excluded by current searches for almost all masses of $m_a$ (see refs.\cite{30,58} for bounds on $f_a$ in other models).

Indirect production of $a$, via the decay $T \to t a$ or $B \to b a$, is therefore an independent test of the models. A dedicated collider study of the signatures is beyond the scope of this article, so we briefly comment on the new allowed final states in a way to relate them to the standard top partner searches. While the BRs shown in figure 2 apply to a specific model, the plot shows some typical behaviours which are generic for most models. We can thus infer a general trend for the dominant final states, depending on the mass range of the $a$:

- For $m_a > 2m_t$, the channel $T \to t a \to tt\bar{t}$ has the dominant BR. This is a generic expectation as long as a sizeable coupling to the tops is present. The resulting “tri-top” and “esa-top” final states are not searched for, but they will be efficiently covered by existing 4-top searches, as shown in ref.\cite{93}.

- Below the $tt\bar{t}$ threshold, the dominant $a$ decays are into hadrons ($gg$) or $b\bar{b}$. Thus, $T \to t a$ decays provide similar final states as standard channels like $T \to t V_{had}$ and $T \to t h \to tb\bar{b}$. However the mass reconstructions applied in current fully hadronic decay searches typically focus on invariant mass reconstructions in the $W/Z$ and Higgs mass ranges. Thus the signal generated by $T \to ta$ is potentially being rejected unless its mass is close to the one of the standard bosons. Note that a simple recast was possible for some Run-I searches where the Higgs mass reconstruction was not imposed\cite{40}.

- The final state $T \to t a \to t\tau^+\tau^-$ could also arise from $T \to t h/t Z$ but is to our knowledge currently not covered by any top partner searches. For VLQ masses much

\footnote{The minor difference in bounds between Bm1 and Bm2 arises mainly from $C_t$-dependent one-loop contributions to $a$ production in gluon fusion, and to a lesser extent from $C_t$-dependent one-loop corrections to the decay partial width of $a$ into $gg$, $Z\gamma$, and $\gamma\gamma$. For expressions of the BRs at one-loop, see ref.\cite{30}.}
larger than $m_t + m_a$, boosted di-tau systems may arise, thus offering interesting final states at the LHC \cite{58, 94, 95}.

- Decays of $a$ to vector bosons (if kinematically allowed) can yield $t\gamma\gamma$, $tZ\gamma$, $tWW$, or $tZZ$ resonances. In our benchmark model(s), these $a$ decays do not have large BRs. Nevertheless, the final states (and the kinematics with a boosted top and a di-boson resonance) offer many handles for excellent SM background rejection.

Similar considerations hold for the VLQ partner $B$.

2.2 Exclusive pNGB, $\tilde{T} \to t\eta$

As a second simplified scenario, we consider a model with a top partner $\tilde{T}$ with charge $2/3$ that does not mix with the SM top, and a lighter pseudo-scalar $\eta$. This situation is realised, for example, in composite Higgs models based on SU(4)/Sp(4) breaking, where $\eta$ is the additional singlet and the top partner couplings respect a parity associated with $\eta$. A concrete realisation will be discussed in section 3.2. The model is described by the Lagrangian

$$L_{\tilde{T}} = \tilde{T} (i\not{D} - M_{\tilde{T}}) \tilde{T} - \left( ik_{\eta,L} \tilde{T} \eta P_L t + L \leftrightarrow R + \text{h.c.} \right), \tag{2.7}$$

for the interactions involving $\tilde{T}$, which differs from eq. (2.1) by the absence of couplings to the SM bosons. For the pseudo-scalar $\eta$, in principle, one can write an effective Lagrangian similar to eq. (2.4). However, in this specific case, not all couplings arise on the same footing. If the couplings of the top respect $\eta$-parity, no couplings of $\eta$ to tops are generated at leading order \cite{96}. The couplings to light fermions are model dependent, but they may also be suppressed; for instance, if they are generated by bilinear couplings, they are absent at the leading order \cite{97}. Thus, to keep the scenario minimal, we will only consider couplings to gauge bosons:

$$L_{\eta} = \frac{1}{2} (\partial_\mu \eta)(\partial^\mu \eta) - \frac{1}{2} m_\eta^2 \eta^2 + \frac{g^2 K^0_{\eta}}{16\pi^2 f_\eta} \eta G^a_{\mu\nu} \tilde{G}^{a\mu\nu} + g^2 K^a_{\eta} \eta W^+_{\mu\nu} \tilde{W}^{-\mu\nu}$$

$$+ \frac{e g W}{16\pi^2 f_\eta} \eta A_{\mu\nu} \tilde{A}^{\mu\nu} + \frac{e g Z}{16\pi^2 f_\eta} \eta Z_{\mu\nu} \tilde{Z}^{\mu\nu} + \frac{e g c}{8\pi^2 f_\eta} \eta A_{\mu\nu} \tilde{Z}^{\mu\nu}, \tag{2.8}$$

for the interactions of $\eta$ with the SM particles.

In the benchmark model we are interested in, as detailed in section 3.2, $\eta$ arises as a singlet from the coset SU(4)/Sp(4) in the EW sector. As a consequence, $K^0_{\eta} = 0$, and the couplings to the EW bosons can be expressed in terms of two parameters, as in eq. (2.5), with the further constraint $K^0_B = -K^0_{\eta}$. Thus, the coupling to photons vanishes, and the BRs are fixed in terms of gauge couplings, as shown in figure 3. To be concrete, we report here the specific values of the couplings in the benchmark model Bm2 discussed in section 3.2:

$$M_{\tilde{T}} = 1.3 \text{ TeV}, \quad k_{\eta,L} = -0.08, \quad k_{\eta,R} = 0.89, \tag{2.9}$$

while for the decay constant, we fix $f_\eta = 1 \text{ TeV}$ and we leave the mass $m_\eta$ as a free parameter. Due to the absence of couplings to gluons and the smallness of the anomaly-induced couplings to EW gauge bosons, $\eta$ by itself is not very visible at the LHC nor at
lepton colliders: production cross sections have been studied in ref. [97] and give very small yields. At loop level, a coupling \( gg \to \eta \eta \) is generated by top-\( \tilde{T} \) loops, and it may give sizeable production rates for small \( \eta \) masses. However, below the \( Z \) mass, the decay rates of \( \eta \) are very model dependent: besides the 3-body decays \( Z^* \gamma \), competitive rates may be due to sub-leading couplings to light quarks or even 3-photon final states generated by anomalous couplings. A detailed study would, however, be required to establish the precise bounds, thus here we will focus on the \( m_\eta > m_Z \) range.

While direct production appears to be negligible, the singlet \( \eta \) will be produced via decays of the top partner \( \tilde{T} \) that can only be pair produced. As in this scenario \( \eta \) decays into EW gauge bosons, the signatures resulting from \( \tilde{T}\tilde{T} \) pair production contain fully-reconstructable 3-body resonances with very low SM backgrounds:

- For \( m_\eta > 2m_W \), \( \eta \) dominantly decays into \( W^+W^- \) which yields a final state of \( pp \to \tilde{T}\tilde{T} \to (tW^+W^-)(\bar{t}W^+W^-) \). Decays into \( ZZ \) and \( Z\gamma \) provide subleading channels.

- Below the \( 2m_W \) threshold, \( \eta \) decays almost exclusively into \( Z\gamma \), providing the interesting final state \( pp \to \tilde{T}\tilde{T} \to (tZ\gamma)(\bar{t}Z\gamma) \).

2.3 Coloured pNGBs: the case \( X_{5/3} \to \bar{b} \pi_6 \)

Models of PC for quarks necessarily contain coloured bound states, as some of the confining underlying fermions need to be charged under \( SU(3)_c \) in order to give colour to the composite top partners. In models with a fermionic underlying description, this implies the presence of coloured pNGBs, which may be lighter than the top partners and can thus appear in top partner decays.\(^6\)

A colour octet pseudoscalar \( \pi_8 \), neutral under the EW interactions, is ubiquitous in models with a fermionic underlying description [30]. It can couple to a quark and quark-partner and therefore appear in quark partner decays, and itself decays into \( t\bar{t}, gg \) or \( g\gamma \).

\(^6\)If a coloured pNGB is heavier than top partners, it can affect their production rates [35].
The presence of $\pi_6$ thus gives rise to final states similar to the ones described in section 2.1 (with the addition of the $g\gamma$ channel).

Other colour charged pNGBs are present in some of the models. Here, we focus on the charge-$4/3$ colour sextet $\pi_6$ [34]. The main reason behind this choice is that it can modify the decays of a charge $5/3$ top partner $X_{5/3}$. The latter is a commonly considered state which is present in top partner multiplets in an SU(2)$_L \times$ SU(2)$_R$ bi-doublet. It is normally assumed to decay exclusively into $t W^+$, which yields a same-sign lepton (SSL) signature from leptonic $W$ decays [98], with low SM background and thus very high sensitivity. $X_{5/3}$ is therefore an ideal target for searches at hadron colliders. Semi-leptonic decays of $t W^+$ have higher background but also a higher BR and provide another attractive channel. For pair-produced $X_{5/3}$, the current bound on its mass is $M_{X_{5/3}} > 1.3\, \text{TeV}$ [45, 99–101], while higher sensitivity for single-produced $X_{5/3}$ is possible, but model-dependent [102]. However, all these bounds assume the absence of “exotic” $X_{5/3}$ decays.

The effective Lagrangian for the $X_{5/3}$ couplings, including the sextet, reads

$$\mathcal{L}_{X_{5/3}}^{\pi_6} = \mathcal{X}_{5/3} \left( i\partial^\mu - M_{X_{5/3}} \right) X_{5/3}$$
$$\quad + \left( \kappa_{W,L}^X g \sqrt{2} \mathcal{X}_{5/3} W^+ P_L t + i\kappa_{\pi_6,L}^X \mathcal{X}_{5/3} \mathcal{X}_{5/3} P_L b^c + L \leftrightarrow R \hspace{1em} \text{h.c.} \right), \quad (2.10)$$
while the one associated to the $\pi_6$ couplings to SM particles is

$$\mathcal{L}_{\pi_6} = |D_\mu \pi_6|^2 - m_{\pi_6}^2 |\pi_6|^2 + \left( i\kappa_{tt,R}^{\pi_6} \bar{t}\pi_6 (P_R t)^c + L \leftrightarrow R \hspace{1em} \text{h.c.} \right), \quad (2.11)$$
where $b^c$ and $t^c$ denote the charge conjugate of the bottom and the top quark fields. Note that, in the model we consider, $\pi_6$ is a singlet of SU(2)$_L$. The coupling $\kappa_{tt,L}^{\pi_6}$ to left handed tops are thus suppressed by $m_t^2/f_{\pi_6}^2$ with respect to $\kappa_{tt,R}^{\pi_6}$. The sextet decays as $\pi_6 \rightarrow t t$, with large dominance to right-handed tops.

The sextet arises, for example, as part of the pNGB spectrum in UV embeddings of composite Higgs models with SU(4)/Sp(4) breaking [34] (see section 3.2). For illustration purposes, we again use this underlying model to define a benchmark model, Bm3, in section 3.3. The values of the couplings are

$$\text{Bm3:} \quad M_{X_{5/3}} = 1.3\, \text{TeV}, \quad \kappa_{W,L}^X = 0.03, \quad \kappa_{W,R}^X = -0.11, \quad \kappa_{\pi_6,L}^X = 1.95, \quad \kappa_{tt,R}^{\pi_6} = -0.56, \quad (2.12)$$
while the other couplings are suppressed, and $f_{\pi_6} = 430\, \text{GeV}$ (note that $f_{\pi_6}$ is not directly related to the compositeness scale for the Higgs, as it comes from a different sector of the theory, and we use here an estimate with respect to a decay constant $f = 1\, \text{TeV}$ in the Higgs sector). The BRs are shown in the left panel of figure 4, demonstrating that sizeable rates into the colour sextet are possible in realistic models.

The phenomenology of $\pi_6$ (in absence of VLQs) has been studied in ref. [34]. It is pair-produced via QCD interactions or singly produced via top-fusion and, following the decay into two top quarks, leads to 4-top final states. At LHC Run I, SSL searches imply a bound of $m_{\pi_6} \gtrsim 800\, \text{GeV}$ [34]. Additional indirect constraints may apply, however they are more model dependent so we conservatively rely on the direct production bound only. The signatures from production via $X_{5/3}$ decays depend on the production mode for the VLQ:
Figure 4. Branching ratios of $X_{5/3}$ and the lightest $T_1$ as a function of $m_{\pi_6}$ in the benchmark model Bm3 introduced in section 3.3.

- For pair produced $X_{5/3}$, the final state contains $tt\bar{t} + bb$, thus it will be efficiently covered by 4-top searches. Additionally, one can have different decays on the two legs, yielding $\bar{b}tW^- + \bar{t}btW^+$, which again matches 4-top searches.

- For singly-produced $X_{5/3}$, the final state will always contain two tops, thus this final state can again be searched for in SSL final states.

While SSL searches seem to efficiently cover this channel, the precise bounds will depend on the different kinematics of the final states. Furthermore, additional requirements, like for instance tagging the b-jets, may improve the reach with respect to standard searches.

Finally, we remark that $\pi_6$ can also couple to other top partners, which can thus decay into it. As $X_{5/3}$ is embedded in an electroweak multiplet (in our example, in an SU(2)$_L \times$ SU(2)$_R$ bi-doublet), additional top partners with mass comparable to $M_{X_{5/3}}$ are generically present. A charge 2/3 top partner can couple to $t \pi_6$, thus adding final states with a $T \rightarrow t \pi_6 \rightarrow itt$ decay. The same final states already occurred in the simplified models in section 2.1, although the kinematics differs, as $\pi_6$ decays into two tops (and not $tt$). Decays of the individual states of the top partner multiplet in our benchmark model Bm3 are discussed in more detail in section 3.3. Here we just give a brief example. In the right panel of figure 4 we show the BRs of the lightest charge 2/3 partner, $T_1$ (with mass $M_{T_1} = 1.3$ TeV) of Bm3 which has a sizeable branching fraction into $\bar{t}\pi_6$, if $\pi_6$ is sufficiently light.

2.4 Charged pNGB, $X_{5/3} \rightarrow t \phi^+$

As a second example for exotic decays of a charge 5/3 top partner, we consider a model with a colour-neutral, electrically charged scalar $\phi^+$. The latter arises for example as part of the pNGB spectrum in composite Higgs models with SU(5)/SO(5) breaking [2] (see section 3.4), where it is accompanied by a doubly-charged scalar. The effective Lagrangians for the VLQ $X_{5/3}$ and the charged scalar couplings, respectively read

$$\mathcal{L}^{\phi}_{X_{5/3}} = \overline{X}_{5/3} \left( i\partial - M_{X_{5/3}} \right) X_{5/3} + \left( \kappa_{W,L}^{X_{5/3}} \frac{g}{\sqrt{2}} \overline{X}_{5/3} W^+ P_L t \right. $$

$$\left. + i\kappa_{\phi^+,L}^{X_{5/3}} \overline{X}_{5/3} \phi^+ P_L t + i\kappa_{\phi^+,L}^{X_{5/3}} \overline{X}_{5/3} \phi^{++} P_L b + L \leftrightarrow R + h.c. \right),$$

(2.13)
Figure 5. Branching ratios of $X_{5/3}$ as a function of the mass of the charged pNGBs $m_\phi = m_{\phi^+} = m_{\phi^{++}}$ for the benchmark model Bm4 introduced in section 3.4.

and\(^7\)

$$
\mathcal{L}_\phi = \sum_{\phi=\phi^+,\phi^{++}} \left( |D_{\mu}\phi|^2 - m_\phi^2 |\phi|^2 \right) + \left( \frac{egK_{W}^{\phi}}{8\pi^2 f_\phi} \phi^+ W_{\mu\nu} \tilde{B}^{\mu\nu} + \frac{g^2 c_w K_{W}^{\phi}}{8\pi^2 f_\phi} \phi^+ W_{\mu\nu} \tilde{B}^{\mu\nu} \\
+ \frac{g^2 K_{W}^{\phi}}{8\pi^2 f_\phi} \phi^{++} W_{\mu\nu} \tilde{W}^{\mu\nu} + i\kappa_{tb,L} \frac{m_t}{f_\phi} \phi^+ P_L b + L \leftrightarrow R + h.c. \right). \quad (2.14)
$$

Note that we have defined a unique decay constant, $f_\phi$, for both charged scalars, as they usually originate from the same coset. In models based on the SU(5)/SO(5) breaking pattern (minimal coset with charged pNGBs), the charged scalar $\phi^\pm$ belongs to SU(2)$_L$-triplets. Thus, in the non-zero hypercharge triplet, a doubly charged scalar $\phi^{\pm\pm}$ is present and has been added to the previous Lagrangians. The latter cannot be neglected, even in this simplified scenario, as it affects the decays of $X_{5/3}$. Thus, the new exotic channels in this scenario are $X_{5/3} \to t \phi^+$ and $X_{5/3} \to b \phi^{++}$. To illustrate these exotic decay modes, we define another benchmark model, Bm4, in section 3.4. The corresponding values of the couplings are given by

Bm4: \quad $M_{X_{5/3}} = 1.3$ TeV, \quad $\kappa^X_{W,L} = 0.03$, \quad $\kappa^X_{W,R} = 0.13$, \quad $\kappa^X_{\phi^+,L} = 0.49$, \quad $\kappa^X_{\phi^{++},L} = -0.69$, \quad $\kappa^\phi_{tb,L} = 0.53$, \quad (2.15)

while the other couplings are suppressed, and $f_\phi = 1$ TeV. The BRs are displayed in figure 5, showing that non-negligible rates into the charged pNGBs $\phi^+$ and $\phi^{++}$ are present in realistic models. Note that we assume for simplicity a common mass $m_\phi$ for the two charged pNGBs.

Due to its anomalous couplings in eq. (2.14), the charged pNGB $\phi^+$ can decay into a pair of SM gauge bosons, either $W^+ \gamma$ or $W^+ Z$. A coupling to $t\bar{b}$ is also generated from PC.

\(^7\)We neglect couplings of pNGBs to leptons and light quarks, which are analogous to the last term of eq. (2.14) and suppressed by $m_t/f_\phi$. Additional couplings may also arise, like lepton number violating ones with the triplet, however their presence is model dependent. As they are not required by the lepton mass generation, we can consistently assume their absence.
Couplings to light fermions are model dependent, as they vary according to the mechanism generating their mass: here, for simplicity, we will neglect them. For the doubly charged pNGB $\phi^{++}$, the only available channel arises from an anomalous couplings to $W^+ W^+$. In the underlying models based on SU(5)/SO(5), the anomalous couplings of $\phi^+$ are related by gauge couplings, as they both originate from the coupling $K_{WB}^\phi$ of the triplet to an SU(2)$_L$ and a U(1)$_Y$ gauge boson. This leads to the relations

$$K_{W\gamma}^\phi = K_{WB}^\phi, \quad K_{WZ}^\phi = -K_{WB}^\phi t_w^2.$$  \hspace{1cm} (2.16)

Below the $t\bar{b}$ threshold, $\phi^+$ mostly decays into $W^+ \gamma$: this is due both to the suppression of the coupling to $W^+ Z$ (shown above) and to the fact that the mass threshold for the $WZ$ channel is very close to the $t\bar{b}$ one. Above the $t\bar{b}$ threshold, the fermionic channel typically dominates. Note that below the $W$ mass, the decays into a virtual $W$ boson (i.e., three body decays) may be competitive with more model dependent decays into light fermions, thus we will not consider this mass region here. It should also be noted that, while dedicated searches are not available, collider bounds on direct production of the charged scalars are very mild: bounds on similar models, which should be applied with a pinch of salt, point towards mass bounds below the $W$ mass [103, 104], so no direct bounds should apply to the mass region we chose. The above scenario leads to different signatures depending on the masses of the charged pNGBs:

- For $m_{\phi^+}$ below the $t\bar{b}$ threshold, the channel $X_{5/3} \rightarrow t \phi^+ \rightarrow tW^+ \gamma$ leads to extra hard photons in addition to the standard final states.

- Above the $t\bar{b}$ threshold, $\phi^+$ decays almost exclusively into $t\bar{b}$, thus offering an interesting final state $X_{5/3} \rightarrow t\bar{b}$ that will be easily covered by the existing 4-top searches when $X_{5/3}$ is pair-produced and both decay into this exotic channel. Different decays on the two legs produce final states similar to four tops, i.e. $tt\bar{b}W^-$ (for one decay through $\phi^+$ and one standard) or $tt\bar{b}W^-W^-$ (for one decay through $\phi^+$ and one through $\phi^{--}$).

- The channel $X_{5/3} \rightarrow b \phi^{++} \rightarrow bW^+ W^+$ leads to a signature similar to the standard $X_{5/3} \rightarrow tW$ (with subsequent top decay to $bW^+$), but with different kinematics.

Finally, let us remark that the charged pNGBs couple in general to the other top partners. The resulting new decay modes are discussed in more details in section 3.4. One interesting final state that we want to mention is due to decays of a charge 2/3 partner in the charged scalar leading to $T \rightarrow b \phi^+ \rightarrow bW^+ \gamma$, which is similar to a top final state with the addition of a hard photon.

3 Exotica in minimal composite Higgs models

The simplified models that describe the new decay modes arise quite naturally in models of a composite Higgs with partially composite fermions. In this section we provide some explicit examples to illustrate the origin of the new channels. We start by providing a simplified scenario where only the minimal matter content is introduced, before analysing two realistic scenarios based on the symmetry breaking patterns SU(4)/Sp(4) and SU(5)/SO(5).
3.1 Simple model of partial compositeness

The main principle behind PC is that elementary fermions linearly couple to vector-like fermion partner states such that they mix, and the lighter eigenstate — which is to be identified with the SM fermion — obtains a mass through electroweak symmetry breaking. This structure appears naturally in composite Higgs models, as the VLQs are identified with composite states themselves. The coupling to the Higgs (as a pNGB) thus arises via the linear mixing operators that connect the elementary fields to the composite fermions.

At an effective model level, the most minimal field content involves two VLQs that have exactly the same quantum numbers as the elementary top fields: an SU(2)\(L\) doublet \(Q = (U, D)\) with hypercharge 1/6, and a singlet \(S\) with hypercharge 2/3. This simple PC Lagrangian, including only linear interactions of the Higgs doublet scalar \(\phi_H\), is given by

\[
- \mathcal{L}_{PC} = M_Q \bar{Q} Q + M_S \bar{S} S + \left( y_L f e^{i \xi_Q} \bar{Q} P_L q + y_R f e^{i \xi_S} \bar{S} P_L S - y_L^\prime \phi_H^\dagger e^{-i \xi_Q} \bar{Q} P_L q + y_R^\prime \phi_H^\dagger e^{-i \xi_S} \bar{S} P_L S + \text{h.c.} \right),
\]

where we have also included the couplings of a pseudo-scalar \(a\) associated to a spontaneously broken global U(1) symmetry with charges \(\xi_{Q,S}\) assigned to the VLQs. Such a pNGB arises naturally in underlying models of PC \([29, 30]\), where an anomaly-free U(1) global symmetry is spontaneously broken by the condensation of underlying fermions. The couplings \(y_{L/R}\) parametrise the linear mixing of the elementary fields with the composite ones, following the PC prescription, while the couplings \(y_{L/R}^\prime\) generate additional mixing terms once the Higgs acquires its vacuum expectation value (VEV). Note that \(y_{L/R}\) generate a mass mixing between fermions with the same SM quantum numbers. They can thus be rotated away to bring eq. (3.1) to a basis which is more familiar to the VLQ literature \([13–15]\) by defining

\[
M_Q' = \sqrt{M_Q^2 + y_L^2 f^2}, \quad s_L \equiv \sin \theta_L = \frac{y_L f}{M_Q'},
\]

\[
M_S' = \sqrt{M_S^2 + y_R^2 f^2}, \quad s_R \equiv \sin \theta_R = \frac{y_R f}{M_S'},
\]

where we remark that the new doublet \(Q'\) and singlet \(S'\) are the genuine VLQs. The couplings of the \(W, Z\) and Higgs can then be obtained diagonalising the full mass matrix, including the electroweak symmetry breaking contributions \([18]\), while the new couplings of the singlet \(a\), following the notation of eq. (2.1), are given by

\[
\kappa_{a,R}^T = \frac{\xi_S M_S'}{f_a} s_R c_R + O(v/M_S'), \quad \text{for the singlet,}
\]

\[
\kappa_{a,L}^T = -\frac{\xi_Q M_Q'}{f_a} s_L c_L + O(v/M_Q'), \quad \text{for the doublet.}
\]

Furthermore, a coupling of the pseudo-scalar \(a\) to two tops is also generated by the diagonalisation of the mass matrix, leading to

\[
g_{att} = -\frac{m_t}{f_a} (\xi_Q s_L^2 + \xi_S s_R^2). \tag{3.4}
\]
Interestingly, this result is different from what we would obtain if we wrote an effective operator generating the mass of the top, as it was done in ref. [30], which would give \( g_{\text{att}} = -i \frac{m_t}{f_a}(\xi_Q + \xi_S) \). This difference is due to the effect of the mixing induced by the VLQs. The fact that the results are truly different can be appreciated if we expand for small Yukawas \((y_{\text{L/R}} \sim y_{\text{L/R}}' \sim y \ll 1)\): the coupling we obtained in eq. (3.4) scales like \( y^4 \) (we recall that \( m_t \sim y^2 \)), while the prediction from the effective operator scales like \( m_t \sim y^2 \).

To understand the physics entailed by the above minimal scenario, it is instructive to study the theory before the Higgs develops its VEV. This is justified as the mass of the VLQs is expected to be much larger than the EW scale (Higgs mass), and we can thus use the equivalence principle to study the couplings of the Goldstone bosons instead of the vector bosons. Calling \( t, T_1, T_2 \) and \( b, B \) the mass eigenstates (without including the Higgs effects), the Lagrangian in eq. (3.1) can be rewritten as

\[
\mathcal{L}_{\text{PC}} = M_Q^2 \left( c_L^2 + s_L^2 e^{i \xi_Q \tilde{\pi}_L} \right) (T_1 P_L T_1 + B P_L B) + M_S^2 \left( c_R^2 + s_R^2 e^{i \xi_S \tilde{\pi}_R} \right) T_2 P_L T_2 \\
+ M_{\text{SS}} s_{LCL} \left( e^{i \xi_Q \tilde{\pi}_L} - 1 \right) (T_1 P_L t + B P_L b) + M_{\text{SS}} s_{RCL} \left( e^{i \xi_S \tilde{\pi}_R} - 1 \right) \phi_P L T_2 \\
+ \left( y_L^L s_{LCL} e^{-i \xi_Q \tilde{\pi}_L} + y_R^L s_{LCL} e^{-i \xi_Q \tilde{\pi}_L} \right) \phi_P L t - \phi^- i P_L b \\
- \left( y_L^L s_{LCL} e^{-i \xi_Q \tilde{\pi}_L} + y_R^L s_{LCL} e^{-i \xi_Q \tilde{\pi}_L} \right) \phi_P T_2 P_L T_1 - \phi^- T_2 P_L B \\
- \left( y_L^L s_{LCL} e^{-i \xi_Q \tilde{\pi}_L} - y_R^L s_{LCL} e^{-i \xi_Q \tilde{\pi}_L} \right) \phi_P T_2 P_L t - \phi^- T_2 P_L b \\
+ \left( y_L^L s_{LCL} e^{-i \xi_Q \tilde{\pi}_L} - y_R^L s_{LCL} e^{-i \xi_Q \tilde{\pi}_L} \right) \phi_P |P L T_1 - \phi^- i P_L B| + h.c. \quad (3.5)
\]

The mass of the top quark is generated by the interaction on the third line of the above equation, allowing us to identify the top Yukawa with

\[
y_{\text{top}} = (y_L^L c_{LCL} + y_R^L s_{LCL}) \quad (3.6)
\]

The couplings of the VLQs to \( a \) and a SM quark, on the other hand, are obtained from the second line after expanding the exponential, thus yielding the results in eq. (3.3). Relying on the equivalence principle, the decay rate of the VLQs into \( a \) can be estimated as follows:

\[
\frac{\Gamma(T_1 \to t a)}{\Gamma(T_1 \to t \phi_0)} = \frac{\Gamma(B \to b a)}{\Gamma(B \to t \phi^-)} = \xi_Q^2 \left( \frac{M_Q^4}{f_a^2} \right)^2 \frac{s_L^2 e_{LCL}^2}{(y_L^L c_{LCL})^2},
\]

\[
\frac{\Gamma(T_2 \to t a)}{\Gamma(T_2 \to t \phi_0) + \Gamma(T_2 \to b \phi^+)} = \xi_S^2 \left( \frac{M_S^4}{f_a^2} \right)^2 \frac{s_R^2 e_{RCL}^2}{2(y_L^L c_{LCL} - y_R^L s_{LCL})^2}. \quad (3.7)
\]

This result clearly shows that the decay rates in the new pseudo-scalar can be substantial, as there is no parametric suppression in their couplings as compared to the couplings to the Higgs field. Furthermore, as long as the charges \( \xi_Q/S \) are non-vanishing, it is not possible to remove the couplings without affecting the mass of the top. To clarify this statement, we can check the result in the limit where the singlet is much lighter than the doublet, i.e. for \( s_L \ll 1 \):

\[
\frac{\Gamma(T_2 \to t a)}{\Gamma(T_2 \to t \phi_0) + \Gamma(T_2 \to b \phi^+)} \approx 0, \quad \frac{1}{2} \xi_S^2 \left( \frac{M_S^4}{f_a^2} \right)^2 \left( \frac{v}{\sqrt{2m_{\text{top}}} + v} \right)^2 s_R^4, \quad (3.8)
\]

which is substantial as long as \( s_R \sim 1 \).
3.2 The SU(4)/Sp(4) scenario

We now analyse explicit models of composite Higgs: we first consider the coset SU(4)/Sp(4), which is the minimal one to enjoy a simple gauge-fermion underlying realisation [9]. The composite VLQs as well as the pNGBs (including the Higgs boson) now originate from a composite sector which is globally invariant under an SU(4) flavour symmetry that is spontaneously broken down to Sp(4). As a consequence, the SM Higgs doublet is accompanied by a pseudo-scalar singlet $\eta$ in order to form a complete representation of the unbroken flavour symmetry. In the same way, the VLQ multiplets must contain additional top partners, whose quantum numbers depend on the choice of the Sp(4) representations.

As a concrete example, we consider two multiplets: one transforming as a 5-plet of Sp(4) and one in the singlet representation. Together they may form a 6-plet of SU(4), and such a top partner easily arises as a “chimera baryon” in underlying models with two species of fermions [20, 21]. Under the SU(2)$_L \times$ U(1)$_Y$ symmetry, the 5-plet decomposes as $2^7/6 + 2^1/6 + 1^2/3$. It thus contains an additional exotic doublet and a singlet together with the SU(2)$_L$ doublet $Q$ of eq. (3.1). The Sp(4) singlet representation, having hypercharge $2/3$, is trivially identified with the singlet $S$ that couples linearly to the right-handed top. The various top partners are labelled as follows:

$$\begin{align*}
5\text{-plet} & \rightarrow \begin{pmatrix} X_{5/3} \\ X_{2/3} \end{pmatrix}, \begin{pmatrix} T \\ B \end{pmatrix}, \tilde{T}_5; \\
singlet & \rightarrow \tilde{T}_1. 
\end{align*}$$

We then introduce a linear mixing of the left-handed top (and bottom) with the doublet contained in the 5-plet and of the right-handed top with the singlet: they are the sources of PC, and their effect can be introduced in the effective Lagrangian in the standard way [7]. In this work, we will follow the same procedure and notations as in ref. [34] to obtain the mass matrices associated to the top partners and the elementary fermions. As we study the couplings to the pNGBs other than the Higgs doublet, we will keep them explicitly in the mass matrix. For the charge $2/3$ fermions, in the basis $\psi_t = \{t, T, X_{2/3}, \tilde{T}_1, \tilde{T}_5\}$, we obtain the following matrix:

$$\begin{pmatrix}
0 & \frac{-y_{5R}e^{i\xi_5}}{\sqrt{2}} f s_\theta & \frac{-y_{5R}e^{i\xi_5}}{\sqrt{2}} f s_\theta & y_{1R} e^{i\xi_1} \frac{\eta}{\sqrt{2}} f c_\theta & i y_{5R} e^{i\eta} \\
y_{5L} e^{i\xi_5} \frac{f}{2} f c_{\theta/2} & M_5 & 0 & 0 & 0 \\
y_{5L} e^{i\xi_5} \frac{f}{2} f s_{\theta/2} & 0 & M_5 & 0 & 0 \\
y_{1L} e^{i\xi_1} \frac{\eta}{\sqrt{2}} f s_\theta & 0 & 0 & M_1 & 0 \\
-iy_{5L} e^{i\eta} \frac{\eta}{2} s_\theta & 0 & 0 & 0 & M_5
\end{pmatrix} \psi_{1L},
$$

where we kept only linear terms in the singlet $\eta$, while the charges $\xi_{1,5}$ can be computed from the underlying theory following ref. [30]. For trigonometric functions we use the shorthand notation $s_\theta = \sin \theta$, etc. The angle $\theta$ is related to the Higgs VEV as $s_\theta \equiv v/f$, and it describes the misalignment of the vacuum in the global flavour space [1]. The matrix
above matches the simplified Lagrangian in eq. (3.1) once we expand for small $\theta$ up to linear terms. Non-linearities, expressed by higher orders in $\theta$ and due to the non-linear nature of the Higgs boson, affect the couplings as follows:

$$M_{S,Q} = M_{1,5}, \quad y_L = y_{5L} e^{\frac{\theta}{2}}, \quad y_R = y_{1R} c_\theta, \quad y'_L = y_{1L}, \quad y'_R = y_{5R},$$  

while a new ingredient is due to the presence of the exotic doublet and of the top partner $\tilde{T}_5$ that couples to $\eta$. For completeness, the matrix for the charge $-1/3$ fermions, in the basis $\psi_b = \{ b, B \}$, is given by

$$\bar{\psi}_b R \begin{pmatrix} 0 & 0 \\ y_{5L} e^{i\xi} \tilde{T}_5 & M_5 \end{pmatrix} \psi_b L, \tag{3.12}$$

while for the exotic charge $5/3$ fermion have mass $M_{X_{5/3}} = M_5$.

The matrix in eq. (3.10), which contains both the mass mixings and the couplings to the two singlets $\eta$ and $a$, has several remarkable features. Firstly, the EW singlet $\tilde{T}_5$ that belongs to the 5-plet of Sp(4) does not mix to other fermions but couples to them via the singlet $\eta$. This is due to the fact that the couplings we wrote preserve a parity [31] under which both $\eta$ and $\tilde{T}_5$ are odd: this parity can be broken if a mixing of the right-handed top to the $\tilde{T}_5$ is added, thus inducing mass mixing and couplings of $\eta$ to all top partners [32]. This will also induce a coupling of $\eta$ to a pair of tops, which is otherwise absent: for an in-depth discussion of the effect of this mixing, we refer the reader to ref. [96], while here we limit ourselves to the simpler case that preserves the parity. Another interesting feature regards the mass ordering inside each multiplet: the composite fermions that mix with the elementary tops receive additional mass contributions from symmetry breaking (analogous to eq. (3.2)). For this reason, within the 5-plet, the components of the SM doublet, $T$ and $B$, tend to be the heaviest, followed by $X_{2/3}$ whose mixings are suppressed by $\theta$, while $X_{5/3}$ and $\tilde{T}_5$ remain degenerate and lighter than the others. The singlet $\tilde{T}_1$, on the other hand, is the lightest state if $M_1 \ll M_5$.\footnote{We use here the notation of the multiplet components to indicate the mass eigenstates with largest superposition with them.} It is important to identify the lightest states as they are most likely to be more copiously produced at colliders and thus first discovered (or more strongly constrained). The final point we want to make regards the bottom quark: its mass is not generated from the matrix in eq. (3.12). Thus, the model needs to be completed by the addition of a partner of the right-handed bottom, or via an effective operator coming from the strong dynamics [106]. In either case, the coupling of the bottom to the strong dynamics is typically smaller than the ones of the top, and we thus neglect this effect. The features we listed here are rather general and also apply for other choices of the top partner representations, and typically even in more general set-ups, as the elementary fields may couple to more than one representation [107].

In the following, we will use the case of a 5-plet and singlet to define benchmark models that can be matched to the simplified models introduced in the previous section 2.

- $\tilde{T}_5 \to t \eta$: The top partner $\tilde{T}_5$ is an ideal candidate for the simplified model in section 2.2, as it only couples to the singlet $\eta$ and it has a 100% BR in $t \eta$. Thus, the
Figure 6. Branching ratios for heavier VLQs as a function of the mass $m_a$ in the benchmark model Bm1 defined in eqs. (3.14) and (3.15). The continuous, dashed and dotted lines correspond respectively to $\mathcal{F} = \{t, T_1, T_2\}$ or $\mathfrak{B} = \{b, B\}$.

decay constant $f_\eta$ defined in eq. (2.8) is equal to $f$, the decay constant of the Higgs. This property is a consequence of our choice to couple the right-handed top to the singlet only, thus preserving a parity associated to the pNGB $\eta$. The couplings of $\eta$ to SM particles also depend on this choice: in fact, the pre-Yukawas we write do not generate a coupling to top nor bottom quarks. Thus, $\eta$-parity is only broken by the Wess-Zumino-Witten (WZW) term, which provides couplings to the EW gauge bosons [8, 97]:

$$L_{WZW} = \frac{d_F c_\eta}{16\sqrt{2}\pi^2 f} \eta \left( g^2 W_\mu^\nu \tilde{W}^{\mu\nu} - g'^2 B_\mu^\nu \tilde{B}^{\mu\nu} \right),$$

(3.13)

where $d_F$ is the dimension of the representation of the underlying fermion under the confining gauge group. Note that additional couplings to the SM fermions may be generated by higher order operators, examples of which can be found in refs. [8, 97]; however, such couplings are small as they come from operators that do not generate the mass of the light fermions, thus inducing $C_f^\eta \ll 1$ (cf. eq. (2.8)). From the WZW term, we see that the singlet $\eta$ can only decay to the final states $W^+W^-, ZZ$ and $Z\gamma$, with rates shown in figure 3.\textsuperscript{11}

Adding an $\eta$-parity violating coupling of the right-handed top to the 5-plet would both induce couplings $\eta t t$ and a mixing of $\tilde{T}_5$ to the top [32], thus this case would match the simplified model in section 2.1. Finally, we remark that the presence of top partners that decay exclusively into $\eta$ also appears for other choices of top partner representations: for instance, for right-handed top into a 5-plet and left-handed top into a 10-plet [96]. In other cases when a $\eta t t$ coupling is inevitable, e.g. when both tops are into a 10-plet [96], this state is absent. Finally, we remark that in some models there might also be a bottom partner that decays exclusively in $\tilde{B} \rightarrow b \eta$.

- $T \rightarrow t a$: the singlet pNGB $a$ derives from a spontaneously broken $U(1)$ global symmetry, that is always present in models of fundamental PC with two representations.

\textsuperscript{11}The WZW term in eq. (3.13) applies to all models with coset $SU(4)/Sp(4)$, however it may be different in other cosets.
As it can be seen in eq. (3.10), all the top partners that mix with the SM fermions have a coupling to the singlet $a$. Furthermore, as discussed in ref. [30], the mass of $a$ only comes from explicit mass terms for the underlying fermions, thus it can be as light as possible. In the following, we will use the models M8 and M9, as defined in ref. [30], as benchmark models, referring the reader to that reference for all details about the models (we just recall that we define $f_a$ following the convention of ref. [58]). The main differences between the two models lie in the decay rates of the singlet $a$, and in the different charges $\xi_{1,5}$ that determine the couplings of $a$ to the top partners.

To guarantee that the lightest partner is one that decays into $a$, we choose benchmark values of the parameters of the model such that the singlet is the lightest, i.e. $M_1 \ll M_5$. We focus on the model M8 (which has larger couplings to $a$), and define the Benchmark model 1 (Bm1) according to the specific values of the input parameters listed below:

$$
\begin{align*}
&M_1 = 600 \text{ GeV}, \quad M_5 = 1.2 \text{ TeV}, \quad f = 1 \text{ TeV}, \\
&B_{\text{Bm1}}: \quad y_{1L} = y_{5L} = 1, \quad y_{1R} = 0.87, \quad y_{5R} = 1.02, \\
&\quad \xi_L = \xi_R = -1.58, \quad f_a = 2.8 \text{ TeV};
\end{align*}
$$

which reproduce the correct value of the top mass.\textsuperscript{12} The resulting spectrum of VLQs reads:

$$
\begin{align*}
&M_{T_1} = 1 \text{ TeV}, \quad M_{\tilde{T}_5} = M_{X_{5/3}} = 1.2 \text{ TeV}, \quad MT_2 = 1.23 \text{ TeV}, \\
&M_B = 1.56 \text{ TeV}, \quad MT_3 = 1.57 \text{ TeV}.
\end{align*}
$$

\textsuperscript{12}While the same masses and pre-Yukawa couplings can be chosen for M9, the values of the charges and decay constant are different: $\xi_L = \xi_R = 0.23, \quad f_a = 1.2 \text{ TeV}.$
Table 2. Same as in table 1 but for the benchmark model Bm2.

|     | $t(b)$ | $T_1$ | $T_2$ | $b(t)$ | $B(T_1)$ | $X_{5/3}(T_2)$ | $\tilde{T}_5 \eta$ |
|-----|--------|-------|-------|--------|-----------|-----------------|-----------------|
| $T_1$ | $5 \cdot 10^{-4}$ | - | - | 0.05 | - | - | - |
| $T_2$ | 0.10 | 2.10^{-8} | - | 0.08 | - | - | - |
| $T_3$ | 0.08 | 1 \cdot 10^{-5} | 5 \cdot 10^{-5} | 0.08 | 0.19 | 0.12 | 0.12 |
| $B$ | 0.14 | - | - | 0.86 | - | - | - |
| $Zt$ | $ZT_1$ | $ZT_2$ | $ht$ | $hT_1$ | $hT_2$ | $hT_1$ | $hT_2$ |
| $T_1$ | 0.40 | - | - | 0.54 | - | - | - |
| $T_2$ | 0.47 | - | - | 0.35 | - | - | - |
| $T_3$ | 0.04 | 0.05 | 0.11 | 0.04 | 0.08 | 0.08 | 0.08 |
| $B$ | - | - | - | - | - | - | - |

Figure 7. Branching ratios for heavier $T_{2,3}$ VLQs as a function of the mass $m_a$ in the benchmark model Bm2 defined in eqs. (3.16) and (3.17). The continuous, dashed and dotted lines correspond respectively to $\Sigma = \{t, T_1, T_2\}$ or $\mathcal{B} = \{b, B\}$. The BRs for the lightest VLQ $T_1$ are reported and discussed in section 2.1, so here we will focus on the heavier states. In figure 6 we show the BRs of the heaviest states $T_3$ and $B$ as a function of the mass $m_a$. We see that in both cases sizeable BRs in the final state $ta$ are present, of the order of 15-20%, while the main rates involve the lightest VLQ $T_1$ and a SM boson. This example shows the importance of chain decays for the searches of heavier states together with the final state containing the new pNGB. For the intermediate mass state $T_2$, the channel $ta$ only amounts to a few percent, while the main channels involve equally $T_1$ and the top quark. Table 1 reports the BRs for all the VLQs in the spectrum for fixed value of $m_a = 15$ GeV, as a reference.

- $B \to b a$: as illustrated in the previous benchmark, if $B$ is heavy it will preferentially decay into a lighter VLQ, thus its phenomenology does not match that of the simplified scenario presented in section 2.1. To obtain a new benchmark model, we lower the value of $M_5$ and reduce $y_{5L}$ in order to reduce the mass split between $B$ and the
lighter VLQs. The benchmark parameters of Benchmark model 2 are:

\[
\text{Bm2: } M_1 = 1.4 \text{ TeV}, \quad M_5 = 1.3 \text{ TeV}, \quad f = 1 \text{ TeV}, \quad y_{1L} = 1.17, \quad y_{5L} = 0.46, \quad y_{1R} = y_{5R} = 1.2, \quad (3.16)
\]

which again reproduce the correct value of the top mass, together with the following VLQ spectrum

\[
M_{T_1} = 1.30 \text{ TeV}, \quad M_{X_1} = M_X = 1.3 \text{ TeV}, \quad M_{T_2} = 1.37 \text{ TeV}, \quad M_B = 1.38 \text{ TeV}, \quad M_{T_3} = 1.85 \text{ TeV}.
\]

The couplings of 8 are calculated for model M8 of ref. [30]. The decays of B are described in section 2.1, while the lightest \( T_1 \) decays in the standard channels. Decays into \( t a \) appear for the heavier \( T_2, T_3 \), whose BRs are shown in figure 7. Finally in table 2 we report the BRs of the whole spectrum for \( m_a = 15 \text{ GeV} \), as a reference.

### 3.3 The SU(4)/Sp(4) × SU(6)/SO(6) scenario

Top partners are, by definition, charged under QCD such that the underlying theory should contain coloured fundamental fermions. This leads to a new sector that, upon condensation, contains coloured pNGBs. While strong bounds apply from QCD production at the LHC, they may still be lighter than the top partners and thus appear in their decays. For models with the Higgs coset \( \text{SU}(4)/\text{Sp}(4) \), it has been shown that the coloured underlying fermions belong to a real representation of the confining gauge group \([20, 21]\), thus an \( \text{SU}(6)/\text{SO}(6) \) pattern of symmetry breaking takes place \([34]\): the theory, therefore, contains 20 additional pNGBs transforming as \( 8_0^c + 6_{4/3}^c + 6_{-4/3}^c \) under \( \text{SU}(3)_c \times U(1)_Y \). The charged colour sextet plays a special role, as it is the only pNGB that can give non-standard decay channels for the exotic charge \( X_{5/3} \), thus we will focus on this channel here (matching the simplified model in section 2.3). The corresponding coupling is given by:

\[
\mathcal{L}_{\pi_6} = i\pi_6 \frac{y_{5L} f}{2 f_X} X_{5/3}^b L b L + \text{h.c.} \quad (3.18)
\]

where \( \pi_6 \equiv \pi^a_6 \lambda^a_6 \) and \( f_X \) is the decay constant associated to the condensate in the new sector \( \text{SU}(6)/\text{SO}(6) \). Note that \( f_X \) corresponds to the decay constant \( f_{\pi_6} \) defined in section 2.3 and its value can be determined on the lattice,\(^{13}\) or be estimated based on the maximally attractive channel hypothesis \([110]\): the latter gives \( f / f_X = 0.38 \) for model M8 and \( f / f_X = 2.3 \) for model M9 \([29, 30]\).

To ensure that \( X_{5/3} \) is one of the lightest top partners, it is enough to consider \( M_1 > M_5 \), without any further assumption on the pre-Yukawas. We further focus on model M9, which has a smaller value for \( f_X \), in order to maximise the BR \( X_{5/3} \rightarrow \overline{b} \pi_6 \) with respect to the standard one \( X_{5/3} \rightarrow t W^+ \). The benchmark model we consider here, therefore, is defined by the following choice of parameters:

\[
\text{Bm3: } M_1 = 1.4 \text{ GeV}, \quad M_5 = 1.3 \text{ TeV}, \quad f = 1 \text{ TeV}, \quad y_{1L} = 1, \quad y_{5L} = 1.2, \quad y_{1R} = 1.1, \quad y_{5R} = 1.05, \quad (3.19)
\]

\(^{13}\)See ref. [108] for results in a different model based on \( \text{SU}(5)/\text{SO}(5) \), and ref. [109] for preliminary results for the model of ref. [20].
Table 3. Branching ratios of the VLQs in the benchmark scenario Bm3 for fixed values of the coloured PNGBs masses, $m_{\pi_6} = m_{\pi_8} = 800$ GeV while $m_a = m_{\eta} = 100$ GeV. The other conventions are the same as in table 1.

Figure 8. Branching ratios of $B$ and $T_2$ as a function of the mass of the coloured pNGBs, $m_\pi = m_{\pi_6} = m_{\pi_8}$, for the benchmark model Bm3 detailed in the text. The continuous, dashed and dotted lines correspond respectively to $\Sigma = \{t,T_1,T_2\}$ or $\mathfrak{B} = \{b,B\}$.

which again reproduces the correct value of the top mass, together with the following VLQ spectrum

$$M_{T_1} = 1.30 \text{ TeV}, \quad M_{T_5} = M_X = 1.3 \text{ TeV}, \quad M_{T_2} = 1.68 \text{ TeV}, \quad M_B = 1.77 \text{ TeV}, \quad M_{T_3} = 1.85 \text{ TeV}. $$

The BRs for the lightest $T_1$ and $X_{5/3}$, which only involve the sextet, are described in section 2.3, so here we focus on the heavier states. For simplicity we assume that the two coloured pNGBs are degenerate, and show the BRs for the $B$ and heavier $T_2$ in figure 8, while numerical values for fixed masses $m_{\pi_6} = m_{\pi_8} = 800$ GeV are show in table 3. Remarkably, the main decay mode involves the colour octet $\pi_8$, which will decay dominantly into $t\bar{t}$, with subleading rates in two gluons and in gluon-photon pair.

3.4 The SU(5)/SO(5) scenario

A scenario with a larger pNGB sector is based on the SU(5)/SO(5) coset, which is present in many models of PC with an underlying completion [21] and yields 14 pNGBs with
quantum numbers $3_{±1} + 3_0 + 2_{±1/2} + 1_0$ under SU(2)$_L \times$ U(1)$_Y$. Thus, in addition to the Higgs doublet and the singlet $η$, the model contains three SU(2)$_L$-triplets: $Φ_0 = (φ_0^0, φ_0^±)$, $Φ_{±1} = (φ_1^0, φ_1^+, φ_1^{++})$ and $Φ_{−1} = φ_{−1}^+, $ with hypercharge 0 and +1 and −1 respectively.

Note that, in general, the two charged scalars, $φ^±_0$ and $φ^+_1$, will mix, while the $φ^0_0$ will mix with the imaginary part of the complex scalar $φ^+_1$ (and with the singlet $η$), which are all pseudo-scalars. This scenario provides the same VLQ exotic decays as in the previous sections (i.e., final states containing $a$, $η$, and coloured pNGBs), but it also offers new decay channels involving the pNGB triplets. In this section, we will focus on the decays to the charged scalars $φ^±_{0,1}$ and $φ^{++}_1$.

Following the explicit model in ref. [22], that corresponds to model M4 [30], we assume that the top partners belong to the fundamental representation of SO(5), which decomposes as $2_{7/6} + 2_{1/6} + 2_{1/3}$ under the EW symmetry and may then couple to both the left and right-handed top quark. In the $ψ_t = \{t, T, X_{2/3}, \bar{T}_3\}$ and $ψ_b = \{b, B\}$ bases (we borrow the same notation as from the previous section) we get the following matrices for the top and bottom sectors respectively (where the U(1) singlet $a$ can be introduced in a straightforward way):

$$
\bar{ψ}_R \begin{pmatrix}
0 & \sqrt{2}y_{5L}f s_θ & \sqrt{2}y_{5R}f s_θ & 2y_{5R}f c_θ \\
2y_{5L}f c_θ^2 & M_5 & 0 & 0 \\
-2y_{5L}f s_θ^2 & 0 & M_5 & 0 \\
\sqrt{2}y_{5L}f c_θ & 0 & 0 & M_5
\end{pmatrix} ψ_L, \quad \bar{ψ}_R \begin{pmatrix}
0 & 0 \\
0 & 2y_{5L}f M_5 \\
0 & 0 & M_5
\end{pmatrix} ψ_b, \quad (3.21)
$$

while for the exotic charged state, we have $M_{X_{5/3}} = M_5$. The lightest top partner, therefore, is always $X_{5/3}$ as it does not receive any contribution to its mass from the Higgs. Note that considering only one VLQ multiplet coupling to both left and right-handed top quarks leads to fewer parameters: one mass $M_5$ and two pre-Yukawa couplings $y_{5L}$ and $y_{5R}$. As before, the mixing pattern of the simplified scenario is recovered for a small misalignment angle $θ$, and we have the following identifications:

$$
M_Q = M_S = M_5, \quad y_L = 2y_{5L}c_θ^2, \quad y_R = 2y_{5R}c_θ, \quad y'_L = -2y_{5L}, \quad y'_R = -2y_{5R}. \quad (3.22)
$$

We will mainly focus on the exotic decays of the $X_{5/3}$ top partner, because it is the lightest state in the multiplet. The allowed decays are $X_{5/3} \rightarrow t \ φ^+_0$, $X_{5/3} \rightarrow b \ φ^{++}_1$, together with the standard $X_{5/3} \rightarrow t \ W^+$, the decay to the doubly-charged scalar is intriguing, but it does not yield truly new final states: the only decay generated by the WZW anomaly is $φ^{++}_1 \rightarrow W^+ W^+$, thus the final state of the exotic $X_{5/3}$ decay is $6W^+ W^+$ like for the standard channel $X_{5/3} \rightarrow t \ W^+$ after the decay of the top quark (although the kinematics differ). On the other hand, both singly charged scalars can decay to $φ^{±}_0 \rightarrow t \bar{b}$ above the $t \bar{b}$ threshold via the PC mixing, and to $φ^{±}_1 \rightarrow W^+ \gamma$ below threshold. Decays to $W^+ Z$ are always suppressed because the threshold is very close to the $t \bar{b}$ one, while below the $W$
mass the decays become more model dependent (a more detailed discussion can be found in section 2.4).

We now discuss some numerical results to show if sizeable BRs to \( X_{5/3} \rightarrow t \phi_{0,1}^+ \) and \( X_{5/3} \rightarrow b \phi_{1}^{++} \) can be achieved.

- \( X_{5/3} \rightarrow t \phi^+/b \phi^{++} \): The exotic charge state \( X_{5/3} \) couples to the charged pNGBs \( \phi_{0,1}^+ \) as well as to \( \phi_1^{++} \). The corresponding couplings are given by:

\[
\mathcal{L}_\phi = i\sqrt{2}y_{5L} \left( \phi_{5/2}^0 s_{\theta/2}^2 + \phi_{1/2}^0 c_{\theta/2}^2 \right) X_{5/3}t_L + iy_{5R}s_\theta \phi_1^- t_R X_{5/3} + i2y_{5L}\phi_1^{++} X_{5/3}b_L + \text{h.c.} \tag{3.23}
\]

As the final states of the decays of the two charged scalars are the same, they cannot be distinguished except for the different kinematics due to their mass. In the following, we work under the assumption that all the non-Higgs pNGBs are degenerate, so it makes sense to consider them as a single particle. The couplings above thus match to the simplified model of section 2.4, defined in eqs. (2.13) and (2.14), provided the identification \( \phi^+ \rightarrow \phi_{0,1}^+ \) and \( \phi^{++} \rightarrow \phi_1^{++} \). We chose to focus on model M4 which has the smallest couplings to \( a \), thus maximising the BRs into the pNGB triplets. The benchmark model we consider here, is defined by the following choice of parameters:

\[
\text{Bm}4:\quad M_5 = 1.3 \text{ TeV}, \quad f = 1 \text{ TeV}, \quad y_{5L} = 0.41, \quad y_{5R} = 0.7, \tag{3.24}
\]

yielding the following VLQ spectrum

\[
M_{T_1} = 1.30 \text{ TeV}, \quad M_{X_{5/3}} = 1.3 \text{ TeV}, \quad M_{T_2} = 1.51 \text{ TeV},
M_B = 1.54 \text{ TeV}, \quad M_{T_3} = 1.92 \text{ TeV}. \tag{3.25}
\]

The BRs for \( X_{5/3} \) are characterised in section 2.4. Here we discuss in more details the benchmark scenario. As already mentioned, \( X_{5/3} \) is always the lightest top partner, and we fix its mass (and consequently \( M_5 \)) to the most conservative experimental bound of 1.3 TeV. The two pre-Yukawa couplings \( y_{5L} \) and \( y_{5R} \) determine the correct value of the top mass and the BRs into the charged pNGBs: in order to maximise the latter, it is not enough to increase \( y_{5L} \) as the mixing in eq. (3.21) changes as well. This fact is behind the choice of values in eq. (3.24).

For the \( X_{5/3} \rightarrow t \phi^+ \) channel, the dominant contribution comes from the left-handed coupling involving \( \phi_1^+ \) as the other couplings are suppressed by the misalignment angle. Here we consider a special situation where the two charged scalars are degenerate and, thus, indistinguishable. In a more general scenario, the mixing between them will share the coupling of \( \phi_1^+ \) to the two mass eigenstates, thus potentially reduce the rate into this channel. Furthermore, if the masses are one below and one above the \( t\bar{b} \) threshold, an interesting situation occurs where both \( X_{5/3} \rightarrow tW^+\gamma \) and \( t\bar{b} \) final states are present.

- \( T \rightarrow b\phi^+ \): The charged pNGBs also couple to the charge 2/3 VLQs \( T_{1,2,3} \). Below the \( t\bar{b} \) threshold, the decay \( \phi_1^- \rightarrow b \phi^+ \rightarrow bW^+\gamma \) occurs and leads to a very interesting
Table 4. Branching ratios of the VLQs in the benchmark scenario Bm4 for fixed values of the pNGB triplet masses, $m_\phi = m_u = m_\eta = 100$ GeV.

| $b(t) \phi_0^3$ | $B(T_1) \phi_0^3$ | $b(t) \phi_1^3$ | $B(T_1) \phi_1^3$ | $t(b) \phi_0^0$ | $\phi_0^0 T_1$ | $T_2 \phi_0^0$ | $t \Re[\phi_0^0]$ | $t \Im[\phi_0^0]$ |
|-----------------|-------------------|-----------------|-------------------|----------------|----------------|----------------|---------------|---------------|
| $T_1$           | $4 \cdot 10^{-4}$ | $4 \cdot 10^{-4}$ | $6 \cdot 10^{-3}$ | $2 \cdot 10^{-4}$ | $0.11$         | $4 \cdot 10^{-3}$ | $4 \cdot 10^{-4}$ | $4 \cdot 10^{-4}$ |
| $T_2$           | $0.23$            | $0.23$          | $7 \cdot 10^{-4}$ | $2 \cdot 10^{-3}$ | $0.15$         | $5 \cdot 10^{-3}$ | $4 \cdot 10^{-5}$ | $4 \cdot 10^{-5}$ |
| $T_3$           | $5 \cdot 10^{-4}$ | $5 \cdot 10^{-3}$ | $2 \cdot 10^{-3}$ | $7 \cdot 10^{-4}$ | $0.15$         | $5 \cdot 10^{-3}$ | $4 \cdot 10^{-5}$ | $4 \cdot 10^{-5}$ |
| $B$             | $8 \cdot 10^{-3}$ | $1 \cdot 10^{-4}$ | $9 \cdot 10^{-3}$ | $1 \cdot 10^{-4}$ | $0.15$         | $5 \cdot 10^{-3}$ | $4 \cdot 10^{-5}$ | $4 \cdot 10^{-5}$ |

$T_1 \Re[\phi_0^0]$ $T_1 \Im[\phi_0^0]$ $T_2 \Re[\phi_0^0]$ $T_2 \Im[\phi_0^0]$ $a(b)$ $T_1 a$ $T_2 a$ $t(b) \eta$ $T_1 \eta$ $T_2 \eta$ $b(t) W$ $B(T_1) W$ $X_{5/3} W(\phi_1^{-})$ $t(b) Z$ $T_1 Z$ $T_2 Z$ $t h$ $T_1 h$ $T_2 h$

|-----------------|-------------------|-----------------|-----------------|-----------------|----------------|----------------|---------------|---------------|
| $T_1$           | $0.03$            | $0.03$          | $7 \cdot 10^{-3}$ | $2 \cdot 10^{-3}$ | $0.03$         | $7 \cdot 10^{-3}$ | $9 \cdot 10^{-4}$ | $10^{-3}$     |
| $T_2$           | $0.03$            | $0.03$          | $7 \cdot 10^{-3}$ | $2 \cdot 10^{-3}$ | $0.09$         | $9 \cdot 10^{-4}$ | $10^{-3}$     |
| $T_3$           | $0.03$            | $0.03$          | $7 \cdot 10^{-3}$ | $2 \cdot 10^{-3}$ | $0.17$         | $5 \cdot 10^{-6}$ | $10^{-3}$     |
| $B$             | $0.03$            | $0.03$          | $7 \cdot 10^{-3}$ | $2 \cdot 10^{-3}$ | $0.14$         | $5 \cdot 10^{-6}$ | $10^{-3}$     |

Figure 9. Branching ratios of $T_1, T_2, T_3$ and $B$ as a function of the common mass of the pNGB triplets $m_\phi$ for the benchmark model Bm4 defined in eqs. (3.24) and (3.25). For simplicity, we assume that all components of the EW triplets have the same mass $m_\phi$. The continuous, dashed and dotted lines correspond respectively to $\Sigma = \{t, T_1, T_2\}$ and $\mathcal{W} = \{b, B\}$.
final state, which features a hard photon together with the standard charged-current final state. Above the threshold, we have \( T \to b \phi^+ \to b t \bar{b} \) with three bottom quarks in the final state when singly produced and six if pair-produced.

As the parameter space is rather constrained due to the presence of few free parameters, we present results here for the same benchmark Bm4 defined above. The BRs for all the \( T \)-partners are shown in figure 9, while table 4 shows, as a references, the values of all channels for a fixed triplet mass of 100 GeV. We see that the dominant decays are into standard channels, with a sizeable component into the neutral pNGBs. As they are taken degenerate here, we group them under a single channel \( \phi_0 \to \eta/\phi_0^0/\phi_1^0/\phi_1^{0*} \): they will decay into a pair of gauge bosons via anomalies plus \( t \bar{t} \) via the PC mixing, thus giving rise to exotic channels characterised by the simplified model of section 2.1 (except for the absence of decays into gluons). The intermediate state \( T_2 \), on the other hand, has sizeable decays into \( b \phi^+ \) (roughly 50%), with the rest shared between standard channels and neutral pNGBs. For completeness we remark that the heaviest one, \( T_3 \), does not decay into any of the triplet pNGBs.

Finally, we report in the bottom-right panel of figure 9 the BRs of the VLQ B (with mass \( M_B = 1.54 \text{ TeV} \)). Besides rather standard decays, it has a sizeable rate into \( X_{5/3}^\pm \phi^- \). The chain decay \( X_{5/3} \to b \phi^{++} \) or \( \to W^+ \), with \( \phi^{\pm \pm} \to W^\pm W^\pm \), gives a final state with four \( W \) bosons plus two \( b \)-quarks if \( X_{5/3} \) is pair-produced.

### 4 Conclusions

The search for heavy VLQs, possibly partners of the top quark, continues to be one of the main physics goals at the LHC. So far, however, the experimental efforts have been concentrated, and limited, to decays to one massive electroweak boson (\( W \), \( Z \) and Higgs) plus a quark, mainly from the third generation. The presence of additional decay channels would forcibly reduce the reach of these searches by adding different final states for which searches are not optimised.

In this article we have proposed four simplified scenarios for additional decay modes for third generation partners, focusing on fermions with charges 2/3 (\( T \)), −1/3 (\( B \)) and 5/3 (\( X_{5/3} \)). These modes are actually rather common in motivated underlying models for composite Higgs with partial compositeness. First we consider decays into a light pseudo-scalar \( a \) in addition to the standard ones, where \( a \) can decay into a pair of gauge bosons via topological anomalies or into a pair of fermions via operators giving rise to the fermion masses. In the underlying theories we consider, the pseudo-scalar is typically associated to an anomaly-free global U(1) symmetry. Secondly, we consider a top partner decaying exclusively into a light pseudo-scalar \( \eta \), which further decays into electroweak gauge bosons. In the underlying models, \( \eta \) originates as an additional pNGB of the Higgs coset. Thirdly, we consider decays of the charge 5/3 partner \( X_{5/3} \) into charged coloured pNGBs. The latter originate from the sector of the underlying theory carrying QCD colour. Finally, decays into additional un-coloured charged pNGBs are considered, also arising from the Higgs coset.
We provide simplified models that can be used for phenomenological studies or to design new searches, while at the same time providing benchmark points coming from realistic underlying models. In all cases, we show that sizeable BRs in the new channels are a norm, rather than a tuned exception, as the parameters we chose are generic. Thus, searches of these new modes are as justified as the ones in the standard channels. The final states we highlight typically contain many top quarks or many electroweak gauge bosons, depending on the mass of the new scalars. They offer, therefore, a rich panorama of final states that can be easily detected at the LHC. Another intriguing class of final states involves hard photons in association to more standard final states: they can occur in the decays of \( \eta \rightarrow Z\gamma \) below the \( WW \) threshold, and decays of the charged scalar \( \phi^+ \rightarrow W^+\gamma \) below the \( t\bar{b} \) threshold. We leave a detailed study of the phenomenology of the new final states for further studies.

Finally, we provide a complete description of the underlying models we use for our benchmarks. An additional interesting point that becomes apparent is that the heavier states also decay into the new light scalars, together with decay chains into the lighter VLQs, thus offering rich (but more complex) signatures that deserve further investigation. Our study shows that the phenomenology of top partners is much richer than what can be described in the most minimal simplified models. The new final states are also a remarkable stamp at collider-accessible energies of the underlying model giving rise to the confining dynamics that may lurk behind the Higgs boson.

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