Abstract—We propose an improvement of the random spreading approach with polar codes for unsourced multiple access, for which each user first encodes its message by a polar code, and then the coded bits are spread using a random spreading sequence. The proposed approach divides the active users into different groups, and employs different power levels for each group in such a way that the average power constraint is satisfied. We formulate and solve an optimization problem to determine the number of groups, and the corresponding user numbers and power levels. Extensive simulations show that the proposed approach outperforms the existing methods, especially when the number of active users is large.

Index Terms—Unsourced multiple-access, polar codes, power allocation, spreading sequences, MMSE estimator.

I. INTRODUCTION

Next generation wireless systems require effective solutions for massive random access motivating the setting of unsourced multiple access (MAC) [1]. In unsourced MAC, a large number of uncoordinated users share a common channel to convey their messages to a central unit. At any given time, only a small subset of all the potential users are active, and the messages are short. Since there is no coordination among the users and there are a very large number of them, there is no user identification, and the users employ the same codebook to transmit their messages (hence the name unsourced MAC). The receiver is only interested in decoding the messages transmitted by the users without any regard to the user identities, and the per-user probability of error (PUPE) criterion is adopted as the performance metric.

The formulation of unsourced MAC and its fundamental limits of communication are developed in [1]. Several low-complexity schemes aiming at reaching the finite-blocklength achievability bounds in [1] are devised in the subsequent literature. These include solutions based on T-fold Aloha [2]–[6], splitting the payload [7]–[9], sparsifying codeword bits [10]–[15], and random spreading [16], [17] approaches.

Among the unsourced MAC approaches, the best performance is obtained by the one based on the random spreading idea in [16], particularly, for the number of active users $K_a \leq 225$. Unlike most papers that use short block length transmissions to deal with interference, [16] considers a scheme where users employ transmissions covering the entire frame. To confront the interference, each user’s message is spread via random sequences. Although the scheme performs very well for relatively low number of active users, its performance deteriorates significantly when $K_a$ exceeds a certain threshold. The reason for the decline in performance is that the interference is treated as noise and the increase in the number of interfering users beyond some threshold becomes excessive.

In another closely related work to our set-up, a polar coding scheme based on sparse spreading is proposed in [11]. The codewords are obtained by different codes of varying lengths, and they are modulated using different power levels. The authors experimentally determine the number of power levels to be used as well as the code lengths and the specific powers. This scheme offers improvements over the solution in [16] for larger number of users, specifically, it outperforms the existing unsourced MAC solutions for $250 \leq K_a \leq 300$.

In this letter, we propose an extension of the random spreading idea in [16] by allowing for the use of different power levels among active users. We formulate an optimization problem to determine the optimal number of power levels as well as their specific values. Each user independently determines which power level to use with a certain probability in such a way to match the optimal power level statistics. We demonstrate that interference is well mitigated by this approach, and the unsourced MAC performance becomes highly superior for a wide range of the number of active users. We also present a simple detector based on an estimate of the covariance matrix of the received signal as an alternative to the one in [16]. Specifically, the reduced performance of the scheme in [16] is ameliorated for $K_a > 225$. The proposed analytical approach can also be used for determining the power levels for the scheme in [11], eliminating the need for extensive numerical experiments for system design. Furthermore, the basic ideas and methodology can potentially be applied to other unsourced MAC schemes as well.

The letter is organized as follows. In Section II, we describe the system model. In Section III, the proposed random access scheme is described. In Section IV, an optimization problem for power allocation (PA) is formulated and solved. Simulation results are provided in Section V, and our conclusions are given in Section VI.

II. SYSTEM MODEL

We consider an unsourced random access model in which $K_a$ out of $K_T$ users are active at a given frame. The number of active users $K_a$ is assumed to be known at the receiver. Each active user transmits $B$ bits of information...
through \(n\) channel uses. Assuming a Gaussian multiple-access channel (GMAC), the received signal vector in the absence of synchronization errors and fading is written as
\[
\mathbf{y} = \sum_{k=1}^{K_u} \mathbf{x}_{ik}(\mathbf{u}_{ik}) + \mathbf{z},
\]
where \(i_k\) is the index of the \(k\)th active user, \(\mathbf{x}_i\) is the length \(n\) spread polar-coded signal corresponding to the message bit sequence \(\mathbf{u}_i \in \{0,1\}^B\) of user \(i\), and \(\mathbf{z} \sim \mathcal{N}(\mathbf{0}, \mathbf{I}_n)\) is the additive white Gaussian noise. Each user selects its message index uniformly from the set \(\{i \in \mathbb{Z} : 1 \leq i \leq 2^B\}\). The average power of each user per channel use is set to \(P\). Therefore, the energy-per-bit of the system can be written as
\[
\frac{E_b}{N_0} = \frac{nP}{2B},
\]
and the PUPE of the system is defined as
\[
P_e = \max \frac{1}{K_u} \sum_{k=1}^{K_u} \Pr(\mathbf{u}_{ik} \notin \mathcal{L}(\mathbf{y})),
\]
where \(\mathcal{L}(\mathbf{y})\) is the list of decoded messages with size at most \(K_u\). The primary purpose is to design encoding and decoding schemes to reach a PUPE less than a target per user error probability \(\epsilon\) with the lowest \(E_b/N_0\).

### III. PROPOSED UNSOURCED MAC SCHEME

#### A. Encoder

The message selected by each user is divided into two parts with \(B_a\) and \(B_c = B - B_a\) bits, i.e., \(\mathbf{u}_i = (\mathbf{u}_{is}, \mathbf{u}_{ic})\). The first part is used to map the preamble bits, \(\mathbf{u}_{is}\), to columns of a signature codebook \(\mathbf{A} \in \mathbb{R}^{n_s \times 2^B}\), where \(n_s\) is the spreading sequence length. Since
\[
P[\exists j \neq i : \mathbf{u}_{ic} = \mathbf{u}_{ja}] \leq \frac{K_u - 1}{2B_a},
\]
\(B_a\) is selected to make the right-hand side of (4) in such a way to satisfy the PUPE requirement. The elements of the matrix \(\mathbf{A}\) are generated by first picking independent zero-mean Gaussian random variables with unit variance, forcing each column to have an average of zero by subtracting its mean from each element, and then scaling them to distinct power levels (the determination of the power levels will be discussed in the following section). Let us denote the column picked by the \(i\)th user by \(\mathbf{a}_i\). The second part of the message, \(\mathbf{u}_{ic}\), is encoded using a polar code. As in [16], this message is appended by \(r\) cyclic redundancy check (CRC) bits, and the result is passed to an \((n_c, B_c + r)\) polar encoder. The CRC bits are used to check the success of polar decoding. The polar codeword is modulated using binary shift keying (BPSK), resulting in \(\mathbf{v}_i \in \{\pm 1\}^{n_c \times 1}\). The transmitted signal for user \(i\) is then obtained as
\[
\mathbf{x}_i = \mathbf{v}_i \otimes \mathbf{a}_i,
\]
where \(\otimes\) represents the Kronecker product.

#### B. Design of the Codebook

While the elements of the codebook \(\mathbf{A}\) are selected in a similar fashion to [16], unlike the codebook in [16] where the empirical variance of all the columns of \(\mathbf{A}\) are normalized, we divide the columns of \(\mathbf{A}\) into \(m\) groups, and assign different power levels to each. There are \(l_k\) columns with power level \(P_k\) in the \(k\)th group, for \(k = 1,2,\ldots,m\). Hence, with a uniform selection, the probability of choosing a column with power \(P_k\) from the codebook is
\[
Pr(\|\mathbf{a}_i\|^2 = P_k) = \frac{l_k}{2B_a}.
\]
Since \(K_a\) active users pick columns of \(\mathbf{A}\) randomly, the number of users with power \(P_k\) can be approximated by
\[
K_k \approx \frac{l_k}{2B_a} K_a,
\]
for \(K_a \gg 1\). Optimization of the codebook parameters \(l_k\) and \(P_k\) is described in the next section.

#### C. Decoder

The decoder is composed of three parts. A newly proposed covariance-based detector identifies the set of spreading sequences employed by the active users; a minimum mean square error (MMSE) estimator is used to produce the soft estimates corresponding to the detected sequences; and finally, the estimated symbols are fed as input to the channel decoder, which is implemented as a polar list decoder. Successive interference cancellation (SIC) is employed to remove the contribution of the successfully decoded messages from the received signal at each step, and the procedure is repeated until the messages of all active users are decoded or there are no successfully decoded users in an iteration.

1) Covariance-Based Detector: As an alternative to the energy detector in [16], which requires searching through possible codeword sequences, we propose an approach which generates an estimate of the covariance matrix of the received signal, and declares the signatures corresponding to the largest diagonal entries as the active ones. Namely, we write the remaining signal after the last SIC step, \(\mathbf{Y}' \in \mathbb{R}^{n_s \times n_c}\), as
\[
\mathbf{Y}' = \mathbf{A}_a \mathbf{V} + \mathbf{Z},
\]
where \(\mathbf{A}_a \in \mathbb{R}^{n_s \times K}\) and \(\mathbf{V} \in \{\pm 1\}^{K \times n_c}\) are constructed by aggregating the signatures and codewords of the \(K\) remaining active users; and, \(\mathbf{Z} \in \mathbb{R}^{n_s \times n_c}\) is the noise matrix with independent and identically distributed zero-mean unit-variance Gaussian random variables as its elements. Note that since via a CRC check, we only remove contributions of the correctly decoded messages at the SIC steps, (8) holds for all the iterations (with the remaining users’ messages). We form
\[
\mathbf{C} = \mathbf{A}_a^T \mathbf{Y}' \mathbf{Y}'^T \mathbf{A}_a^T
\]
where \(\mathbf{A}_N\) is obtained by scaling the columns of the codebook to 1 to prevent higher detection probability for the sequences with greater power levels. The covariance-based detector outputs \(K_r = K_f + K_\delta\) signatures corresponding to largest diagonal elements of \(\mathbf{C}\), where \(K_f\) is the number of remaining users up to the current iteration and \(K_\delta\) is a small integer.
Let us comment on the complexity of the proposed approach. The number of multiplications required to calculate the diagonal entries of matrix \( C \) in (9) is \( N_c = n_s^2 n_r + 2B_t n_s + 2B_s n_r \), while the number of multiplications required in the energy detector [16] is \( N_c = n_s n_r 2^{(g + B_s)} \). Here \( g \) denotes the length of each partition in the energy detector. Clearly, for moderate values of \( g \), e.g., for \( g = 8 \), the complexity of the energy detector is significantly higher than that of the newly proposed one. For small \( g \) values, however, the complexities of the two approaches are similar.

2) Channel Decoder and SIC: Accumulating the signatures declared by the covariance-based detector in the matrix \( \hat{A}_D \in \mathbb{R}^{n_s \times (K + K_s)} \), the MMSE estimate of \( \hat{V} \) is obtained by [16]

\[
\hat{V} = \hat{A}_D^T \hat{C}_y^{-1} \hat{Y}',
\]

with \( \hat{C}_y = (I_{n_s} + \hat{A}_D \hat{A}_D^T) \), where the \( i \)th row of \( \hat{V} \) (denoted by \( \hat{v}_i \)) is the estimated codeword of user \( i \). We treat \( \hat{v}_i \) as the output of an AWGN channel with noise variance \( \hat{\sigma}_s^2 \), where \( \hat{\sigma}_s^2 \) is obtained by picking the \( i \)th diagonal entry of the mean square error (MSE) matrix, MSE = \( \hat{A}_D^T \hat{C}_y^{-1} \hat{A}_D \). The \( i \)th user’s message is then decoded by feeding \( \hat{d}_i = 2\hat{v}_i/\hat{\sigma}_s^2 \) to the list decoder.

After polar decoding, the successfully decoded codewords that satisfy the CRC check are removed from the received signal. The residual received signal is then passed back to the covariance-based detector for the next iteration. This procedure is repeated until there are no successful decoding results or all the active users are decoded.

We finally note that decoding of users with low power levels are adversely affected in the presence of users with higher power levels. To alleviate this effect, we run the decoder \( m + 1 \) times with indices \( i = 0, 1, \ldots, m \). At the \( i \)th step, the signatures of the \( i \) groups with the larger power levels are removed from the codebook when using the covariance-based detector. Therefore, the matrix \( \hat{A}_D \) does not have the spreading sequences with high power levels in it, which makes the decoding of signals with lower power levels easier as the high-power interfering signals are removed. The details of the decoding procedure are given as a pseudo-code in Algorithm 1.

IV. DESIGN OF SPREADING SEQUENCES: OPTIMAL POWER ALLOCATION

A. Selection of Optimal Parameters

Suppose that active users are divided into \( m \) groups consisting of \( K_1, K_2, \ldots, K_m \) users with power levels \( P_1 \leq P_2 \leq \cdots \leq P_m \), where \( K_1 + K_2 + \cdots + K_m = K \). Note that during the interference cancellation procedure, the users with the highest power levels are expected to be decoded first. Focusing on (5), we notice that \( x_i \) is obtained by normalizing a zero-mean Gaussian vector, hence we model the aggregate interference as a Gaussian random vector added to each user’s signal. For instance, for the group with the highest power level, \( K_m \) users with power \( P_m \) experience interference with variance \( \sigma_m^2 = 1 + K_1 P_1 + K_2 P_2 + \cdots + K_m \) after successful decoding and interference cancellation of the group \( m \) users, we decode the \( K_{m-1} \) users with power level \( P_{m-1} \), which experience interference with variance \( \sigma_{m-1}^2 = 1 + K_1 P_1 + K_2 P_2 + \cdots + K_{m-1} P_{m-1} \). From (23) in Appendix VI, the minimum required power for the \( j \)th group becomes

\[
P_j = \frac{\alpha_{\min}(K_j)}{1 - (K_j - 1)\alpha_{\min}(K_j)} \left(1 + \sum_{i=1}^{j-1} K_i P_i\right),
\]

which can be rewritten as

\[
P_j = \gamma_j \prod_{i=1}^{j-1} (1 + K_i \gamma_i) \quad \forall j = 1, 2, \ldots, m,
\]

where \( \gamma_j = \frac{\alpha_{\min}(K_i)}{1 - (K_j - 1)\alpha_{\min}(K_j)} \), and \( \alpha_{\min}(K_j) \) is the minimum required signal-to-interference-plus-noise ratio (SINR) for achieving a target PUPE in a group with \( K_j \) users. Note that \( \alpha_{\min}(K_j) \) depends on the particular coding and transmission scheme employed, and can be determined via simulations. Therefore, the total power can be written as a function of \( K_1, K_2, \ldots, K_m \) as

\[
P_T = K_1 P_1 + K_2 P_2 + \cdots + K_m P_m = \prod_{i=1}^{m} (1 + K_i \gamma_i) - 1.
\]

We can find values of \( K_1, K_2, \ldots, K_m \) which minimize the total power by solving the following optimization problem:

\[
(K_1, \ldots, K_m) = \arg \min \ P_T, \quad \text{s.t.} \quad \sum_{i=1}^{m} K_i = K. \quad (14)
\]

To proceed further, we relax the integer constraint on \( K_j \)’s, and use the method of Lagrange multipliers. The cost function to be minimized is

\[
J(K_1, \ldots, K_m) = \prod_{i=1}^{m} (1 + K_i \gamma_i) + \lambda \left( \sum_{i=1}^{m} K_i - K \right),
\]

\[
\text{Algorithm 1 Pseudo-Code for the Decoder Steps}
\]

**Input:** \( Y, \hat{A}, \text{and } K_a. \)

**flag = 1**, \( K_r = K_a, \ Y' = Y. \)

**while** \( flag = 1 \) **do** Decoding

**for** \( i = 0, 1, \ldots, m \) **do**

- \( i \) groups with higher powers are removed from \( \hat{A}_N. \)
- \( S = \emptyset. \)
- \( \hat{A}_D \) is the output of covariance-based detector.
- Compute \( \hat{V} = \hat{A}_D^T \hat{C}_y^{-1} \hat{Y}'. \)
- Feed \( \hat{d}_i = 2\hat{v}_i/\hat{\sigma}_s^2 \) to the list decoder.
- Update \( S \) as the set of decoded codewords.
- \( K_r = K_j - |S| \) and \( K_s = K_x + |S| \).
- \( Y' = Y' - \hat{A}_S \hat{V}_S. \)

**if** \( K_s \geq 1 \) **then**

**end**

**break.**

**if** \( K_r = 0 \) **or** \( K_r = 0 \) **then**

**flag = 0.**

**end**
where $\lambda$ is the Lagrange multiplier. Setting the derivative of the Lagrangian to zero gives

$$\frac{K_1 \gamma_i' + \gamma_i}{1 + K_1 \gamma_i} = \frac{K_2 \gamma_2' + \gamma_2}{1 + K_2 \gamma_2} = \cdots = \frac{K_m \gamma_m' + \gamma_m}{1 + K_m \gamma_m} = -\frac{\lambda}{P_T + 1}. \quad (16)$$

Strictly speaking, while $\alpha_{\text{min}}(K_i)$ is a function of $K_i$, this value is almost a constant (for a given target PUPE level). Dropping this dependence, after some calculations, we obtain

$$K_i \gamma_i' + \gamma_i = \frac{\alpha_{\text{min}}}{1 + K_i \gamma_i}, \quad (17)$$

where $\alpha_{\text{min}}/(1 - (K_i - 1)\alpha_{\text{min}})$ is a one-to-one function of $K_i$, the optimal values of $K_i$ satisfy $K_1 = K_2 = \cdots = K_m = K_0$, with $K_0 = K_a/m$. We can also argue that (with a constant $\alpha_{\text{min}}$), the Hessian for $J(K_1, \ldots, K_m)$ is given as

$$\nabla^2(J) = (P_T + 1)\text{diag}\left(\frac{K_1 \gamma_1'' + 2 \gamma_1''}{1 + K_1 \gamma_1}, \ldots, \frac{K_m \gamma_m'' + 2 \gamma_m''}{1 + K_m \gamma_m}\right)$$

with

$$\gamma_i' = \frac{\partial \gamma_i}{\partial K_i} = \left(1 - (K_i - 1)\alpha_{\text{min}}\right)^2, \quad (19)$$

$$\gamma_i'' = \frac{\partial^2 \gamma_i}{\partial K_i^2} = 2 \left(1 - (K_i - 1)\alpha_{\text{min}}\right)^3, \quad (20)$$

where $\text{diag}(\zeta_1, \ldots, \zeta_l)$ is an $l \times l$ diagonal matrix with the $i$th diagonal element $\zeta_i$. From (23), we observe that $\alpha_{\text{min}}/(1 - (K_i - 1)\alpha_{\text{min}})$ is proportional to the minimum required power, which is always positive. Thus, the Hessian in (18) is a positive definite matrix, and (14) is verified to be a convex optimization problem.

Determining that the number of users in all the groups should be the same, we can optimize this quantity as

$$m = \min_m \left(1 + \frac{K_a \gamma_0}{m}\right)^m. \quad (21)$$

B. General Case

We highlight that, even though the optimal PA approach is applied to the random spreading scheme, the basic ideas can also be extended to other unsourced MAC scenarios (for which the interference is treated as noise) by solving (21) for the specific $\alpha_{\text{min}}(K)$ values.

V. NUMERICAL RESULTS

In this section, we study the performance of the proposed approach and compare it with other existing solutions for unsourced MAC. The total number of channel uses is selected as $n \approx 30000$ ($n_a = 117$ and $n_c = 256$), the number of active users is $150 \leq K_a \leq 600$, the list size for the polar decoder is $L = 512$, and the target PUPE is set to $P_T = 0.05$. The number of information bits per message is chosen as $B = 100$, where $B_a$ is selected as $B_a = 14$ for $150 \leq K_a < 200$, $B_a = 15$ for $200 \leq K_a \leq 250$, $B_a = 16$ for $250 < K_a \leq 350$, $B_a = 17$ for $350 < K_a \leq 500$, and $B_a = 18$ for $500 < K_a \leq 600$.

Note that, the probability that three or more users are in collision is very small for the selected values of $B_a$, hence their effects can be neglected. Also, as discussed in [16], the random spreading scheme with channel coding rate lower than $1/2$ is able to resolve the possible collision of two users, providing a good performance.

To obtain $\alpha_{\text{min}}(K_0)$ for the random spreading scheme, the method in [16] is run for different values of $K_a$, and the result is shown in Fig. 1(a) for $B_a = 14$ and 18. One should keep in mind that the required SINR must be computed for different values of $B_a$ separately, as this value is sensitive to $B_a$ in the random spreading scheme. Plugging $\alpha_{\text{min}}(K_0)$ into (21), the optimal number of groups, $m$, is obtained (as depicted in Fig. 1(b)). Clearly, for $K_a \leq 125$, only one group should be employed, however, beyond that number of users, employing more than one group with different power levels becomes optimal.

We also apply our approach to the sparse spreading idea of [11] to determine the optimal number of groups and the corresponding power levels without any need for extensive simulations. The results are depicted in Fig. 1. We compare the required $E_b/N_0$ of the scheme in [11], the random spreading scheme in [16], the sparse spreading solution with optimal PA, and the random spreading approach with optimal PA in Fig. 2. It can be inferred from this result that employing the optimal PA for the random spreading scheme decreases the required $E_b/N_0$ of the system remarkably, especially, for the larger number of active users, i.e., for $K_a > 225$. Moreover, it is shown that the required $E_b/N_0$ is the same for the sparse spreading scheme via the analytically obtained PA and the sparse spreading scheme in [11] where the parameters are empirically chosen.

In Fig. 3, the performance of the proposed random spreading solution with optimal PA is compared with the other existing unsourced MAC schemes. The result clearly indicates that the proposed method offers superior performance, particularly, when the number of active users is large.
sparse spreading scheme [11], the random spreading scheme [16], the sparse spreading with optimal PA, and the random spreading with optimal PA.

We further note our observation that the detection probability of the covariance-based detector is slightly higher than that of the energy detector for manageable values of $g$, and for the specific parameters of $n_s$, $n_c$, and $B_s$ in this section. Regarding its complexity, for $K_a = 500$ and $B_s = 17$, the total number of multiplications required by the proposed covariance-based detector and the energy detector with $g = 1$ are $N_c = 1.81 \times 10^9$ and $N_e = 7.85 \times 10^9$, respectively. That is, the computational complexity of the covariance-based detector and energy detector with $g = 1$ are comparable.

VI. CONCLUSION

We have studied unsourced MAC with polar codes and random spreading, and developed an approach which divides the active users into multiple groups with different transmit power levels. The number of groups and the power levels are selected through a suitably formulated optimization problem, and it is shown by numerical evaluations that the idea of using different power levels provides a significant reduction in the required $E_b/N_0$, particularly, for systems with a large number of active users.

APPENDIX

THE MINIMUM REQUIRED POWER IN EACH GROUP

Since we are treating interference as noise, from the perspective of a user, the SINR becomes the important performance metric. In a group with $K_j$ users with power level $P_j$, and noise variance $\sigma_j^2$, we need

$$\alpha_{\min}(K_j) \leq \frac{P_j}{\sigma_j^2 + (K_j - 1)P_j}. \quad (22)$$

Since our objective is to minimize the total power, we can select the power level for each user as

$$P_j = \frac{\alpha_{\min}(K_j)}{1 - (K_j - 1)\alpha_{\min}(K_j)}\sigma_j^2. \quad (23)$$

REFERENCES

[1] Y. Polyanskiy, “A perspective on massive random-access,” in Proc. IEEE Int. Symp. Inf. Theory (ISIT), Aachen, Germany, Jun. 2017, pp. 2523–2527.
[2] R. Calderbank and A. Thompson, “CHIRRUP: A practical algorithm for unsourced multiple access,” Inf. Inference, J. IMA, vol. 9, no. 4, pp. 875–897, Dec. 2020.
[3] A. Vem, K. R. Narayanan, J. Cheng, and J.-F. Chamberland, “A user-independent serial interference cancellation based coding scheme for the unsourced random access Gaussian channel,” in Proc. IEEE Int. Theory Workshop (ITW), Kaohsiung, Taiwan, Nov. 2017, pp. 121–125.
[4] A. Vem, K. R. Narayanan, J.-F. Chamberland, and J. Cheng, “A user-independent successive interference cancellation based coding scheme for the unsourced random access Gaussian channel,” IEEE Trans. Commun., vol. 67, no. 12, pp. 8258–8272, Dec. 2019.
[5] O. Ordentlich and Y. Polyanskiy, “Low complexity schemes for the random access Gaussian channel,” in Proc. IEEE Int. Symp. Inf. Theory (ISIT), Aachen, Germany, Jun. 2017, pp. 2528–2532.
[6] E. Marshakov, G. Balitskiy, K. Andreev, and A. Frolov, “A polar code based unsourced random access for the Gaussian MAC,” in Proc. IEEE 90th Veh. Technol. Conf., Honolulu, HI, USA, Sep. 2019, pp. 1–5.
[7] V. K. Amalladinne, A. Vem, D. K. Soma, K. R. Narayanan, and J.-F. Chamberland, “A coupled compressive sensing scheme for unsourced multiple access,” in Proc. IEEE Int. Conf. Acoust., Speech Signal Process. (ICASSP), Calgary, CA, USA, Apr. 2018, pp. 6628–6632.
[8] V. K. Amalladinne, J.-F. Chamberland, and K. R. Narayanan, “A coded compressed sensing scheme for coordinated multiple access,” 2018, arXiv:1809.04745. [Online]. Available: http://arxiv.org/abs/1809.04745
[9] A. Fengler, P. Jung, and G. Caire, “SPARCs for unsourced random access,” IEEE Trans. Inf. Theory, vol. 67, no. 10, pp. 6894–6915, Oct. 2021.
[10] A. Pradhan, V. Amalladinne, A. Vem, K. R. Narayanan, and J.-F. Chamberland, “A joint graph based coding scheme for the unsourced random access Gaussian channel,” in Proc. IEEE Global Commun. Conf., Waikoloa, HI, USA, Dec. 2019, pp. 1–6.
[11] M. Zheng, Y. Wu, and W. Zhang, “Polar coding and sparse spreading for massive unsourced random access,” in Proc. IEEE 92nd Veh. Technol. Conf., Victoria, BC, Canada, Nov. 2020, pp. 1–5.
[12] D. Truhachev, M. Bashir, A. Karami, and E. Nassaji, “Low-complexity coding and spreading for unsourced random access,” IEEE Commun. Lett., vol. 25, no. 3, pp. 774–778, Mar. 2021.
[13] A. K. Tanc and T. M. Duman, “Massive random access with trellis-based codes and random signatures,” IEEE Commun. Lett., vol. 25, no. 5, pp. 1496–1499, May 2021.
[14] Z. Han, X. Yuan, C. Xu, S. Jiang, and X. Wang, “Sparse Kronecker-product coding for unsourced multiple access,” 2021, arXiv:2103.04722. [Online]. Available: http://arxiv.org/abs/2103.04722
[15] J. R. Ebert, V. K. Amalladinne, S. Rini, J.-F. Chamberland, and K. R. Narayanan, “Stochastic binnning and coded demixing for unsourced random access,” 2021, arXiv:2104.05686. [Online]. Available: http://arxiv.org/abs/2104.05686
[16] A. K. Pradhan, V. K. Amalladinne, K. R. Narayanan, and J.-F. Chamberland, “Polar coding and random spreading for unsourced multiple access,” in Proc. IEEE Int. Conf. Commun. (ICC), Dublin, Ireland, Jun. 2020, pp. 1–6.
[17] A. K. Pradhan, V. K. Amalladinne, K. R. Narayanan, and J.-F. Chamberland, “LDPC codes with soft interference cancellation for uncoordinated unsourced multiple access,” 2021, arXiv:2105.13985. [Online]. Available: http://arxiv.org/abs/2105.13985