Investigating AGN Black Hole Masses and the $M_{BH}-\sigma_e$ relation for Low Surface Brightness Galaxies

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ABSTRACT

We present an analysis of the optical nuclear spectra from the active galactic nuclei (AGN) in a sample of low surface brightness (LSB) galaxies. Using data from the Sloan Digital Sky Survey (SDSS), we derived the virial black hole (BH) masses of 24 galaxies from their broad $H\alpha$ parameters. We find that our estimates of nuclear BH masses lie in the range $10^5 - 10^7 M_\odot$, with a median mass of $5.62 \times 10^6 M_\odot$. The bulge stellar velocity dispersion $\sigma_e$ was determined from the underlying stellar spectra. We compared our results with the existing BH mass - velocity dispersion ($M_{BH}-\sigma_e$) correlations and found that the majority of our sample lie in the low BH mass regime and below the $M_{BH}-\sigma_e$ correlation. We analysed the effects of any systematic bias in the $M_{BH}$ estimates, the effects of galaxy orientation in the measurement of $\sigma_e$ and the increase of $\sigma_e$ due to the presence of bars and found that these effects are insufficient to explain the observed offset in $M_{BH}-\sigma_e$ correlation. Thus the LSB galaxies tend to have low mass BHs which probably are not in co-evolution with the host galaxy bulges. A detailed study of the nature of the bulges and the role of dark matter in the growth of the BHs is needed to further understand the BH-bulge co-evolution in these poorly evolved and dark matter dominated systems.

Key words: galaxies: active - galaxies: nuclei - galaxies: bulges - galaxies: general

1 INTRODUCTION

Low surface brightness (LSB) galaxies are late type galaxies that have a central disk surface brightness of $\mu_{B}(0) \geq 22$ to 23 mag arcsec$^{-2}$ (Impey & Bothun 1997; Impey, Burkholder & Sprayberry 2001; Das 2013). Optically they are distinguished by their diffuse, low luminosity stellar disks. The LSB disks have low star formation rates and are low in metal content (McGaugh 1994; Impey & Bothun 1997). Morphologically they span over a wide range of galaxies from dwarfs and irregulars to very large disk galaxies (McGaugh, Schombert & Bothun 1995). However loosely they can be divided into two types the (i) LSB dwarf and irregular galaxies and (ii) disk LSB galaxies. The LSB dwarfs and irregulars form the larger fraction of LSB galaxies and can be found in different environments such as galaxy groups or even within voids (Pustilnik et al. 2011). Disk LSB galaxies are more rare and usually found in low density environments (Bothun et al. 1993) and vary over a range of sizes (Beijersbergen, de Blok & van der Hulst 1999). But the LSB galaxies with really large disk scale lengths (like Malin 1 which has a scale length of 55 kpc, Bothun et al. 1987), referred to as giant LSB (GLSB) galaxies, are generally found to lie close to the edges of voids (Rosenbaum et al. 2009). A recent study by Shao et al. (2015) on the environment, morphology and stellar populations of a sample of bulgeless LSB galaxies suggest that their evolution may be driven by their dynamics including mergers rather than by their large scale environment. Another defining characteristic of all LSB galaxies is their large H$\alpha$ gas content. Large or small, LSB galaxies usually have large HI disks that can extend over several optical disk scale lengths (de Blok, McGaugh & van der Hulst 1996; O'Neil et al. 2004; Das et al. 2007). The HI rotation curves clearly show that their disks are dark matter dominated (Fickering et al. 1977) and even their centers have significant dark matter content (Kuzio de Naray, McGaugh & de Blok 2008). The
dark matter halo can suppress the formation of disk instabilities such as bars and spiral arms, which slows down the rate of star formation in these systems (Mayer & Wadsley 2004, Ghosh & Joshi 2014).

Nuclear activity is not common in LSB galaxies. This is in marked contrast to high surface brightness disk galaxies where the percentage having active galactic nuclei (AGN) can be as high as 50%, depending on the mean luminosity of the sample (Ho, Filippenko & Sargent 1997). The most probable explanation for this low fraction is that LSB disks generally lack two structural features that facilitate inward gas flows and the formation of a central mass concentration in galaxies - bars and strong spiral arms in disks (Bothun, Impey & McGaugh 1997). These structural features may be suppressed by the dominant dark matter content in these galaxies (Ghosh & Joshi 2014). Most of the GLSB galaxies have significant bulge component along with the large LSB disk (Beijersbergen, de Blok & van der Hulst 1999). Whereas a large fraction of normal LSB disk galaxies are relatively bulgeless (McGaugh & Bothun 1994). But there is often a bright core due to nuclear star formation which appears as a luminous point in a featureless low luminosity disk (Matthews et al. 1999). Strong Hα and [O i] emission lines in their spectra indicate ongoing nuclear star formation which is often in the form of kiloparsec (kpc) scale rings, as observed in the galaxy NGC 5905 (Comerón et al. 2010; Raichur et al. 2013; Raichur et al. 2014). Hubble space telescope (HST) observations have shown that the nuclear star formation can lead to the formation of compact nuclear star clusters that may sometimes co-exist with AGN activity (Seth et al. 2008). This activity can contribute to the formation of a central massive object (CMO) and lead to the build up of a bulge in an otherwise bulgeless galaxy (Davies, Miller & Bellovary 2011).

However, although we do not generally see AGN in LSB galaxies, a significant fraction of bulge dominated GLSB galaxies do show AGN activity (Sprayberry et al. 1995; Galaz et al. 2011). Some of them are even radio bright and visible in X-rays (Das et al. 2004; Naik et al. 2011; Mishra et al. 2013), Galaz et al. (2011) compared the stellar mass, radius, absolute magnitude and the red shift distributions of LSB galaxies and High Surface Brightness (HSB) galaxies hosting AGN. They found that most of the distributions for LSB galaxies and HSB galaxies are similar, except the distribution of petrosian radius, r90. AGN activity in bulge dominated GLSB galaxies is not surprising as studies indicate that the growth of nuclear black holes (BHs) in galaxies is intimately linked to the growth of their bulges (e.g. Silk & Rees 1998, Heckman et al. 2004a). The strong correlation of BH mass (MBH) with bulge mass or bulge luminosities in galaxies (MBH - σe) is due to this super massive black hole (SMBH) - bulge co-evolution (Gilbrekin et al. 2009 and McConnell & Ma 2013). But in LSB galaxies, their bulge velocity dispersion and disc rotation speeds suggest that they lie below the MBH - σe correlation for bright galaxies (Pizzella et al. 2003). X-ray studies also suggest that GLSB galaxies do not lie on the radio X-ray correlation (Das et al. 2004) and their BH masses may be quite low (Naik et al. 2011). Mei, Yuan & Dong (2009) estimated the BH masses of three GLSB galaxies and found them to lie close to the MBH - σe correlation and the values of MBH are found to be in the order of \( \sim 10^7 \, M_\odot \). But later, the estimates from the study of another three GLSB galaxies by Ramya, Prabhu & Das (2011) showed that their sample galaxies lie offset from the MBH - σe correlation, with MBH values of 3.9 \( \times 10^5 \, M_\odot \).

Thus these studies suggest that LSB galaxies tend to have low mass BHs \( \sim \, 10^7 \, M_\odot \) and some of them lie below the MBH - σe correlation. A systematic study of a larger sample of LSB galaxies is needed to show a convincing trend.

Ramya, Prabhu & Das (2011) suggested that the bulges of their sample might be well evolved, but the MBH values are lower than those found in bright galaxies. Beijersbergen, de Blok & van der Hulst (1999) could not find any distinction between the structural parameters (bulge to disk ratio and size) of the bulges in the LSB galaxies and normal galaxies. Morelli et al. (2012) found that the stellar populations in the bulges of LSB galaxies have similar properties as that of the bulges of normal galaxies. Based on this they concluded that the formation and evolution history of bulges in LSB galaxies are similar to that of the bulges in normal galaxies. Pizzella et al. (2008) found signatures of pseudo bulges in 6 galaxies with LSB disk. Kormendy & Ho (2013) and references therein suggest that these pseudo bulges do not correlate with BHs in the same way as classical bulges correlate. The two LSB galaxies, UGC 6614 and Malin 2 studied by Ramya, Prabhu & Das (2011) which lie off from the MBH - σe relation are more likely to host classical bulges (Das 2013, Schmitz et al. 2014). If they host classical bulges then the reason of their observed offset is not clear. The significant contribution of dark matter in the inner regions may also affect the growth of the BHs in these systems. The total sample of bulge dominated LSB galaxies with AGN activity, specifically studied so far is very small (6 galaxies) to say any statistically significant trend on the mass of the BHs, their location in the MBH - σe correlation and the nature of the bulges they host. Though some of the LSB galaxies have been analysed in other studies of a large sample of AGN dominated systems (BH mass estimates for the galaxies, 1226+0105 and LSBC F727-V01, are available from Greene & Ho 2007), there is no specific study dedicated to analyse a large sample of LSB galaxies and to understand the BH-bulge co-evolution in these systems. A systematic study of a large sample of LSB galaxies is needed to understand the AGN activity, typical range of MBH values, nature of their bulges and the BH-bulge co-evolution in these poorly evolved and dark matter dominated systems. Low mass BHs in isolated LSB galaxies are also very interesting candidates for the study of seed BHs in galaxies (Valuteri 2011).

In this paper, we present a detailed analysis of 24 bulge dominated LSB galaxies with signatures of type - I AGN (broad Hα component) identified from a large sample of 558 LSB galaxies to understand the AGN activity and to estimate the mass of the BHs present in their centers. Based on their location in the MBH - σe plot and from the nature of their bulges we discuss the presence/absence of BH-bulge co-evolution in these systems. In the following sections (Section: 2 and Section: 3) we discuss the sample and analysis. The results are described in Section: 4. Discussion and conclusions are presented in Sections: 5 and 6 respectively.
2 DATA AND SAMPLE

The Sloan Digital Sky Survey (SDSS) Data Release 10 (DR10) include hundreds of thousands of new galaxy and quasar spectra from the Baryon Oscillation Spectroscopic Survey (BOSS), in addition to all imaging and spectra from prior SDSS data releases. The spectral range of the SDSS multi-object spectrograph and the BOSS spectrograph is almost similar and the spectra resolution is $\sim 70$ km/s for both instruments. The SDSS spectrograph fibre aperture is $3$ arcsec in diameter (corresponding to $2.9$ kpc at a redshift of $0.05$) and the fibre aperture of BOSS spectrograph is $2$ arcsec in diameter (corresponding to $1.9$ kpc at a redshift of $0.05$). Thus the size of the nucleus/bulge sample in the BOSS spectra will be less than that of the SDSS spectra.

The literature (Impey et al. 1996, Sprayberry et al. 1995, Schombert & Bothun 1988, Schombert et al. 1992, Burkholder, Impey & Sprayberry 2001, Galaz et al. 2002) provides a large sample ($\sim 1200$) of LSB galaxies. As an initial sample we selected a sample of $558$ LSB galaxies from the literature, mentioned above, for which the SDSS DR10 nuclear spectra are available. The emission line fluxes of these $558$ galaxies are available for public in the SDSS DR10 database. The Galspec product in the SDSS database provides the emission line fluxes for SDSS-I/II galaxies estimated based on the methods given by Kauffmann et al. (2003a), Brinchmann et al. (2004) and Tremonti et al. (2004). The emission line fluxes for SDSS III BOSS spectra are provided by the team in University of Portsmouth (Thomas et al. 2013).

The H$\alpha$, H$\beta$, [N$\text{ii}_6583$] and [O$\text{iii}_{5007}$] emission line fluxes of the $558$ galaxies, were extracted from SDSS database using SQL query and the [N$\text{ii}_6583$/H$\alpha$] vs [O$\text{iii}_{5007}$/H$\beta$] Baldwin-Phillips-Terlevich (BPT) first given by Baldwin, Phillips & Terlevich (1981) and improved further by Veilleux & Osterbrock (1987), also see Kewley et al. (2003) and Kewley et al. (2004) and references therein) diagram is constructed. This is shown in Figure 1. The solid line is the starburst-Seyfert demarcation line taken from Kauffmann et al. (2003a) and the dotted line represents the extreme starburst line taken from Kewley et al. (2001). This is used as our primary diagnostic to select the AGN candidates for our further investigation. The sample to the left of solid line are considered as pure star forming galaxies and the sample to the right of the dotted line are considered as pure AGN candidates. The sample between the two lines are classified as composite. For these galaxies the nuclear activity can be due to both star formation and AGN activity.

![Figure 1](image_url)  
Figure 1. The BPT AGN diagnostic diagram,[O$\text{iii}$]/H$\beta$ versus [N$\text{ii}$/H$\alpha$] for the sample of $558$ galaxies. The emission line fluxes for these sample galaxies are taken from the SDSS database. The solid line is the starburst-Seyfert demarcation line taken from Kauffmann et al. (2003a) and the dotted line represents the extreme starburst line taken from Kewley et al. (2001). The sample to the left of the solid line are considered as pure star forming galaxies and the sample to the right of the dotted line are considered as pure AGN candidates. The sample between the two lines are classified as composite. For these galaxies the nuclear activity can be due to both star formation and AGN activity.

mate of $\sim 29\%$ is including the composite and AGN sample. If we consider only the sample which are classified as pure AGN candidates, the fraction is $\sim 16\%$. This value is closer to the estimates of Mei, Yuan & Dong (2004) who found a fraction of $10$-$20\%$ LSB galaxies have AGN.

From the sample of $160$ galaxies (which constitute the purely AGN candidates and composite candidates) we are particularly interested in those which host broad H$\alpha$ emission. The broad H$\alpha$ emission line full width at half maximum (FWHM) and luminosity can be used to estimate the masses of active BHs in the centers of these galaxies (Reines, Greene & Geha 2013). To identify the sample with broad H$\alpha$, good quality spectra are required and hence, out of $160$ galaxies we selected only those galaxies which have median S/N $> 15$. Thus, finally we used an initial sample of $115$ SDSS DR10 spectra of LSB galaxies to identify sources with broad balmer lines, specifically the H$\alpha$ line which is the strongest balmer emission line in the optical wavelength region. The steps involved in the analysis of these $115$ galaxies are described in the next section.

3 ANALYSIS

3.1 Spectral Decomposition

In order to isolate the AGN emission lines and identify the sample with broad H$\alpha$ feature, we first removed the
spectral contribution from underlying stellar population. The observed spectra of 115 galaxies were corrected for galactic reddening using the E(B-V) values provided by Schlafly & Finkbeiner (2011). Then we used the pPXF (Penalized Pixel-Fitting stellar kinematics extraction) code by Cappellari & Emsellem (2004) to obtain the best fit model for the underlying stellar population. The emission lines in the observed spectra were masked and the several masked spectra were modelled as a combination of single stellar population templates of different ages. The MILES single stellar population models are used as templates of the underlying stellar population. The templates are available for a large range of metallicity ([M/H] ~ -2.32 to +0.22) and age (63 Myr to 17 Gyr). pPXF uses Gauss-Hermite parametrisation (Gerhard 1993; van der Marel & Franx 1993) and works in the pixel space, which makes it easy to mask gas emission lines or bad pixels from the fit and the continuum matching can be done directly (Cappellari & Emsellem 2004). pPXF creates an algorithm with initial guesses for systemic velocity of the system, V (redshift, z) and stellar velocity dispersion, σ. The model spectra are convolved with a broadening function using initial σ values. The residuals of each of the data points are fed into a non-linear least squares optimization routine to obtain V, σ and Gauss-Hermite polynomials. Though the major contribution to the observed spectra is the underlying stellar population, there are other contributors like power law continuum from AGN, Fe lines etc. While estimating the best fit to the underlying population, ppxf fits a polynomial, along with the optimal template, to account for the contributions from power law continuum. And the Fe lines in these galaxies are too weak to affect our further analysis. In all our sample galaxies the stellar population contribution to the best fit ranges from 80 - 95 % and the remaining factor is the contribution from AGN continuum and Fe lines. The output of this step of analysis is shown in the bottom panel of Figure: 2 (for the galaxy Malin 1 with identification number, 13). The reddening corrected spectra is shown in black and the best fit model is overplotted in red colour. The best fit model is subtracted from the reddening corrected spectrum to get the pure emission line spectrum (the residue of the pPXF fit).

Figure 2. The bottom panel shows the pPXF fit for the galaxy, Malin 1 (identification number 13). The black line is the observed spectrum and the red line is the best fit optimal template for the underlying stellar population. The Gaussian fits to the different emission lines are shown in upper left and upper right panels. The black line is the reddening corrected pure emission line spectra and the red line is the fit to the spectra. The blue lines show the separate components of the spectral region. The residue of the fits are also shown in the upper panels. In the upper right panel, the reduced χ² values of the fits with and without (inside the parenthesis) broad Hα component are shown.
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Table 1. Basic parameters of the sample which are flagged as galaxies with broad Hα component. The distances shown here are the luminosity distances taken from NED. The weight of de Vaucouleurs component to the total, (de Vaucouleurs + Exponential component), fit which is a proxy for the B/T ratio is obtained from the SDSS DR10 database. Bulge Sersic index, n_b is taken from Simard et al. [2011].

| No | Galaxy               | Morphology   | Galaxy Coordinates | Distance (Mpc) | fracDev | n_b |
|----|----------------------|--------------|--------------------|----------------|---------|-----|
| 1  | 1226+0105 or 2MASX J12291286+0049042 | Sc           | 12°29'12.8'' +00°49'04.7'' | 349 | 1.0 | 7.95 |
| 2  | VII Zw 318            | Sc (Merging pair?) | 13°30'32.0'' -00°36'14.5'' | 237 | 0.87 | 1.43 |
| 3  | 2MASX J14334627+0106576 | Sc           | 14°38'46.3'' +01°06'58.8'' | 365 | 1.0 | 7.47 |
| 4  | Leda 135884           | Sb           | 23°15'01.7'' +00°04'24.7'' | 214 | 0.61 | 7.97 |
| 5  | NGC 7589              | SAB(rs)a     | 23°18'15.7'' +00°15'40.3'' | 120 | 0.98 | 5.91 |
| 6  | UGC 00568             | Sd           | 00°55'08.9'' -01°02'47.4'' | 189 | 1.0 | 4.88 |
| 7  | 2MASX J00534265-0105066 | Sbc        | 00°53'42.6'' -01°05'07.5'' | 193 | 1.0 | 6.36 |
| 8  | UGC 00514             | Sb           | 00°50'42.7'' +00°25'58.0'' | 291 | 0.34 | 8.0 |
| 9  | LSB F611-03           | Sc           | 01°13'20.1'' +14°43'40.0'' | 180 | 1.0 | 5.35 |
| 10 | ZW 091               | Interacting  | 10°37'23.8'' +02°18'43.4'' | 173 | 0.93 | 3.41 |
| 11 | ZW 43                | Sc(r)        | 14°36'02.0'' +02°51'06.0'' | 124 | 1.0 | 8.0 |
| 12 | LSB F727-V01         | Sc           | 15°51'40.5'' +08°52'52.0'' | 307 | 1.0 | 6.16 |
| 13 | Malin 1              | S            | 12°36'59.3'' +14°19'49.0'' | 366 | 1.0 | 5.62 |
| 14 | UGC 10050            | Spiral       | 15°49'44.9'' +18°31'37.9'' | 58.7 | 1.0 | – |
| 15 | LSB F500-V01         | Spiral       | 10°23'33.1'' +22°47'46.3'' | 320 | 0.98 | 5.06 |
| 16 | NGC 0926             | SB(s)bc      | 02°26'06.7'' -00°19'55.5'' | 86  | 0.56 | – |
| 17 | UGC 09087            | S0           | 14°12'16.8'' +18°17'58.5'' | 74.5 | 0.91 | – |
| 18 | UGC 08828            | Spiral       | 13°54'26.8'' +21°49'48.4'' | 120 | 0.38 | – |
| 19 | 2MASX J10255577+0200154 | SBB       | 10°25'55.7'' +02°00'16.0'' | 304 | 0.93 | 6.24 |
| 20 | IC 2423              | SAB(s)bc     | 08°54'47.4'' +02°13'13.3'' | 132 | 1.0 | – |
| 21 | LSB F564-01          | Galaxy Pair  | 09°10'29.4'' +20°33'53.5'' | 123 | 1.0 | 5.16 |
| 22 | SDSS J130370.64+202627.3 | Spiral    | 10°37'04.9'' +20°26'27.0'' | 184 | 1.0 | 3.87 |
| 23 | 2MASX J14565122+2152295 | Spiral    | 14°56'51.2'' +21°52'30.0'' | 195 | 0.70 | 8.0 |
| 24 | UGC 09614            | SA(r)a       | 11°39'14.9'' +17°08'37.0'' | 93.2 | 1.0 | – |
| 25 | LSB F508-02          | Sb           | 13°06'59.0'' +22°44'15.5'' | 150 | 1.0 | 4.21 |
| 26 | KUG 0012-000         | Sb           | 00°14'55.1'' +00°15'08.0'' | 160 | 0.57 | 3.68 |
| 27 | CGCG 006-023         | Spiral       | 09°16'13.7'' +00°42'02.2'' | 166 | 0.98 | 8.0 |
| 28 | UGC 06284            | Galaxy pair  | 11°15'49.1'' +00°51'36.0'' | 200 | 0.89 | 3.53 |
| 29 | LSB F573-04          | Sb           | 12°18'15.2'' +20°00'49.0'' | 127 | 0.42 | 5.77 |
| 30 | UGC 09355            | SBA          | 09°27'10.2'' +21°35'38.5'' | 161 | 1.0 | 5.4 |

3.2 Emission line analysis

The pure emission line spectra are carefully analysed by modelling the narrow lines and simultaneously looking for the presence of broad balmer line profiles. Broad balmer lines indicate the presence of dense gas orbiting the central BH within the broad line region. For the sample with broad balmer lines, M_BH can be estimated using scaling relations. The Ho line is the strongest balmer line in the optical wavelength region and hence to identify the final sample with broad balmer lines, we analysed the spectra of the initial sample in the wavelength range, 6400-6880 Å. As the Ho line is blended with the [Ni] doublet, we need to carefully fit this region to extract the broad line component of Ho.

The method adopted here is similar to that described in Reines, Greene & Geha (2013). The method is based on the assumption that the [Si] doublet lines close to the Ho region and well separated, are a good representation of the shape of the [Ni], Ho and Hβ narrow lines. The [Si] doublet is fitted with a single Gaussian model with the width of the two lines assumed to be equal and the relative separation between the two lines held fixed by their laboratory wavelengths. The [Si] model is used as a template to fit the narrow Ho and [Ni] doublet lines. The Ho + [Ni] region of our emission line galaxy spectra are first modelled with three Gaussian components, one for Ho narrow and two for [Ni] doublet. The widths of [Ni] lines are assumed to be the same as that of [Si] lines. The separation between the centroids of the [Ni] narrow components are held fixed using laboratory wavelengths and the flux of [Ni]λ6583 to [Ni]λ6548 is fixed at the theoretical value of 2.96 Ludwig et al. (2012). The reduced χ^2 value for the fit is obtained. Then the region is again fitted including a fourth component representing the broad Ho line. The final sample with broad Ho component is selected based on the three criteria, that the the inclusion of the broad component should improve the reduced χ^2 value by at least 10%, the broad Ho FWHM should be greater than 600 kms^{-1} (after correcting for the instrumental resolution) and also the broad Ho peak flux should be at least two times larger than the residue of the fit. Thus based on the above criteria, 30 LSB galaxies were flagged as galaxies with broad Ho component. The basic parameters of these 30 galaxies are given in Table 1. More careful examination of the model fits of each of these 30 galaxies are performed before making the final sample of broad line AGN candidates for which the BH masses are estimated. This is described in Section: 4. 3.

The other emission lines present in the spectra of these 30 galaxies were also analysed. The narrow line profile derived from the [Si] doublet is also used as a template for fitting Hβ, using the same approach as that for Ho. The
Hβ line is fit twice, with and without a broad component. Here the width of broad Hβ line is assumed to be the same as that of the broad Hα line. Based on the same criteria used to identify the broad component in Hα, the broad component in Hβ is also identified. Since the [O iii] profile commonly exhibits a broad, blue shoulder (Heckman et al. 1981; Whittle 1985), the [O iii] doublet are fitted independently with one or two Gaussian components (the two component model is included if the reduced χ² improves by 10 %). The [O i] doublet lines are also independently fitted with single Gaussian component. We have used the standard ‘MPFITFUN’ of IDL to fit the emission lines employing the ‘GAUSS1’ program where the parameters need to be fit for each Gaussian are centroid, peak value and sigma(fwhm/2.35). The input parameters are wavelength, flux and sqrt(1/inverse variance of flux) as error. The fitting routine provides the best fitting parameters are wavelength, flux and sqrt(1/inverse variance of flux) as error. The fitting routine provides the best fitting parameters along with errors associated with these parameters. The fluxes of all the emission lines are estimated using the peak and sigma values provided by the fit. Uncertainties in the fitted parameters of peak and sigma are added in quadrature to obtain the error on fluxes. The forbidden narrow emission line fluxes of 30 galaxies are tabulated in Table A1. The different emission line profile fits of the galaxy, Malin 1 (with identification number 13) are shown in the upper right and upper left panels of Figure 2.

4 RESULTS

4.1 BPT Classification

As described in Section 2, the initial sample of AGN candidates (which includes the broad line AGN candidates) were selected based on their location in the [O iii]/Hβ versus [N ii]/Hα AGN diagnostic diagram (Figure 1). After further analysis we found that of these only 30 galaxies have an extra-broad component in their Hα emission region along with their narrow lines. The narrow emission line fluxes of these 30 galaxies are estimated after carefully deconvolving them from the other components. In this section, we discuss the location of the sample galaxies in the three AGN diagnostic diagrams. In Figure 3, we revisit the location of these 30 galaxies in the primary diagnostic diagram, [O iii]/Hβ versus [N ii]/Hα. From the figure, we can see that 7 galaxies are in the composite region and the remaining 23 galaxies are in the AGN region. Further classification of the sample into Seyfert/LINER are made using the other two AGN diagnostic diagrams, [O ii]/Hβ versus [S ii]/Hα and [O iii]/Hβ versus [O i]/Hα. These diagrams are shown in Figures 4 and 5. The demarcation lines between starbursts, Seyferts and LINERs were obtained from Kewley et al. (2001), Kewley et al. (2000) and Kauffmann et al. (2003a) and are shown in these diagrams. The [O iii]/Hβ versus [O i]/Hα plot shown in Figure 5 has only 25 points as the remaining 5 galaxies do not have [O i] in emission. The galaxies, 1, 2, 5, 8, 12, 21 and 23 (~ 20% of the sample) are classified as Seyfert type based on Figures 4 and 5. The galaxies in the starburst region in Figure 4 (26, 27 and 29) and Figure 5 (26, 27) are those which are classified as composite in Figure 3. The galaxy with identification number 29 is not present in Figure 5 as it does not have [O i] in emission. The galaxy, 17 which is classified as LINER in Figure 4 lies closer to the starburst/Seyfert demarcation line in Figure 5. This discrepancy may be due to the very low amount of flux (with relatively large error) associated with the [O i] emission line for this galaxy (see Table A1).

4.2 Metallicity of the sample

The [N ii]λ6583, [O iii]λ5007, Hα and Hβ narrow emission line fluxes are used to estimate the oxygen abundance of the nu-
clear/bulge regions of the final sample using the empirical relation derived by Pettini & Pagel (2004). The relation is given as, 

\[ 12 + \log (O/H) = 8.73 - 0.32 \times \text{O3N2}, \]

where \( \text{O3N2} \) is defined as \( \log \left( \frac{[\text{O III}/H\beta]}{[\text{N II}/H\alpha]} \right) \).

Here we would like to mention that the estimated metallicities are gas phase metallicity. The metallicity distribution of the sample galaxies is shown in Figure 6 and the metallicity value has a range, from \( \log[O/H] = 7.94 \) to 8.8. The mean metallicity is \( \sim 8.6 \), which is only slightly lower than the solar value of 8.69 (Asplund et al. 2009). A few of the galaxies with identification numbers, 26, 18, 16 and 6 in the sample are slightly super solar. This initially appears surprising as LSB galaxies are generally low in metallicity. However, these results are derived from nuclear spectra. Nuclear star formation may result in higher metallicities in the central regions compared to the disks of LSB galaxies. Hence due to recent star formation in the central regions, the metallicity is probably higher than the disks of LSB galaxies. The underlying stellar population obtained from pPXF fits, of these four super solar metallicity galaxies, except the galaxy with identification number 18, have contributions from young (500 Myr-2 Gyr) and metal rich (M/H = 0.00 to 0.22) population.

4.3 Broad line AGN candidates

From Section: 3.2 we found that 30 galaxies were identified to host AGN with broad H\( \alpha \) component in their emission line spectrum. Each of these 30 galaxies were examined carefully to define a sample of broad AGN candidates. Out of 30, 3 galaxies (with identification numbers, 26, 27 and 29) are classified as star forming galaxies (Figures: 3, 4 and 5). This may be due to the reason that the star formation dominated the narrow emission lines within the SDSS fibre and the underlying broad component is real. But the broad component in H\( \alpha \) may as well be due to the contribution from stellar phenomenon. In these three galaxies, the broad component detection was marginal and we removed them from our final secure sample of broad line AGN candidates.

The broad H\( \alpha \) component of other two galaxies (identification numbers, 28 and 30, Figures: 17 and 18) are significantly blue shifted (15 - 17 Å which is \( \sim 10 - 11 \) times the error associated with the central wavelength) which can be more likely to be associated with an outflow event rather than with a BH accretion. One of these galaxies (identification number 28) has a similar blueward component in [O III] along with the blue shifted H\( \alpha \) balmer line, which also supports the presence of outflow. These two galaxies are also removed from our final sample. For the remaining 25 sample galaxies, except the galaxy with identification number 2, the central wavelengths of the broad and narrow H\( \alpha \) components are separated by less than 3 times the error associated with the line centers. For the galaxy with identification number 2, the broad and narrow components are separated by \( \sim 6 \) times the error associated with the line centers and the broad component is blue shifted. This galaxy also shows a blue shifted outflow signature in [O III]. It can be assumed that for the galaxy, 2 the broad H\( \alpha \) component may have contribution from both the broad line region due to BH accretion and from an outflow. We could not deconvolve the components due to the outflow and due to BH accretion using numerical profile fitting. Another galaxy, UGC 6614 (identification number 24) has a clear signature of outflow, blue shifted component in [O III] doublet lines as well as in H\( \alpha \) and H\( \beta \) emission lines, along with a broad H\( \alpha \) component. The candidates (identification number 2, 24, 28 and 30) with outflow signatures are discussed in Section: 5.3.

In order to check whether the broad H\( \alpha \) feature is due to the over subtraction of the H\( \alpha \) absorption line, we modelled the H\( \alpha \) absorption line of each sample (obtained from the best fit model, Section: 3.1) with a single Gaussian and ob-
tained the FWHM. The FWHM of Hα absorption line in our sample galaxies is less than 600 kms$^{-1}$, which is one of the criteria to identify the broad Hα component. For all our sample galaxies except the galaxy, LSBC F500-V01, the FWHM of broad Hα component is above ∼ 2-3 times the FWHM of the Hα absorption line. For LSBC F500-V01 (with identification number, 15), the FWHM of the Hα absorption line is 550 kms$^{-1}$ and the FWHM of broad Hα is 995±286 kms$^{-1}$. Also, the absorption line fit has large residue in the wings. Thus the broad Hα component of this galaxy may not be real. As the two values are comparable and the absorption line fit is poor, we removed this galaxy from our final sample of broad line AGN candidates. The broad Hα detection in other sample galaxies appears to be real and not due to the over subtraction of Hα absorption line. Thus we have 24 confirmed broad line AGN candidates for which the mass of the BH can be estimated using scaling relations. Out of 24 broad line AGN candidates, 8 of them (∼ 30%) showed the presence of broad Hβ component as well. The broad line parameters are given in Table A2. The emission line fits, similar to Figure: 2, of some of the remaining galaxies are shown in Section: 5.4 and the rest in appendix, A1.

4.4 Mass of the Central Black Hole

The virial $M_{BH}$ of 24 broad line AGN candidates was calculated using the equation given in [Reines, Greene & Geha (2013)], using the luminosity and FWHM of broad Hα. The equation is given below.

$$\log \frac{M_{BH}}{M_\odot} = 5.57 + 0.47 \log \frac{L_{H\alpha}}{10^{47} ergs s^{-1}} + 2.06 \log \frac{FWHM_{H\alpha}}{10^3 km s^{-1}}$$

In the original equation given in [Reines, Greene & Geha (2013)] the term $\log(\epsilon)$ in the right hand side is the scale factor that depends on the broad line region geometry. There is a range of values available in the literature for $\epsilon$ (∼ 0.75 - 1.4). We have used $\epsilon = 1$. The variation in the estimated $M_{BH}$ values with the adopted values of $\epsilon$ and its effect on the observed $M_{BH} - \sigma_e$ correlation is discussed in Section: 5.1.

The masses estimated are in the range $4.8 \times 10^5 M_\odot$ - $3.6 \times 10^7 M_\odot$. The median mass was found to be $5.62 \times 10^6 M_\odot$. The median mass is in the low end of the SMBH mass regime. These low mass BHs in the poorly evolved and isolated LSB galaxies are good candidates to study the evolution of heavy seed BHs. The mass distribution is shown in Figure: 7. The figure shows that the LSB galaxies have an asymmetric distribution in their BH masses, with a sharp decrease in the galaxies with BH masses less than $10^6 M_\odot$. This can be due to the selection effect on the sample. The two galaxies with BH masses less than $10^6 M_\odot$ are good candidates to study the nature of seed BHs in galaxy nuclei. The Eddington ratio of these accreting BHs are estimated using the bolometric luminosity estimated from [OIII]$_{5007}$ flux. The value associated with each galaxy is given in Table A2.

4.5 $M_{BH}$ vs $\sigma_e$ plot

The stellar velocity dispersion values obtained using pPXf were corrected for aperture effects due to the finite size of SDSS fibre. The equivalent velocity dispersion $\sigma_e$ at a radius of $r_e/8$ in the galaxy bulge, where $r_e$ is the effective radius of the bulge, is calculated using the transformation equation given by [Jorgensen, Franx & Kjaergaard (1993)]. The effective radius of the bulge corresponding to each galaxy in our sample is obtained from the SDSS database where
a de Vaucouleurs profile is fitted to the surface brightness profile and the effective radius of the bulge is obtained. The BH mass estimates for the 24 galaxies in our sample plotted against the equivalent velocity dispersion values, $\sigma_e$ are shown in the $M_{BH} - \sigma_e$ plot in Figure: 8. Also plotted in the figure are the linear regression lines given by [Tremaine et al. 2002], [Ferrarese & Merritt 2000], [Gültekin et al. 2009], [Kormendy & Ho 2013] for only classical bulges/elliptical galaxies and [McConnell & Ma 2013] for late type galaxies (dashed, solid, dotted, short-long dashed and long-dashed lines, respectively) for $M_{BH}$ against $\sigma_e$, based on a quiescent galaxy sample. The $M_{BH} - \sigma_e$ relations obtained for AGN sample appears to be shallower/flatter than that obtained for inactive/quiescent galaxies [Woo et al. 2011, Greene & Ho 2006].

The slopes of active and inactive sample are consistent only within 2$\sigma$ level. [Woo et al. 2013] found that this discrepancy is due to inherent selection effects in the observed sample and intrinsically the $M_{BH} - \sigma_e$ relations for both the active and inactive galaxies are similar. [Xiao et al. 2011] investigated the low mass end of the $M_{BH} - \sigma_e$ relation of active galaxies and found that they tend to follow the extrapolation of the $M_{BH} - \sigma_e$ relation of inactive galaxies. Hence we use only the scaling relations obtained from quiescent galaxy sample as reference frame for the comparison of our sample.

From the plot we can see that most of the galaxies are offset from the $M - \sigma_e$ correlation. Here we would like to point out that the errors given with the $\sigma$ values are obtained from the pPXF fit. The default errors given by pPXF are known to be an underestimate of the true uncertainty associated with the $\sigma$. But even an increase in the errors obtained from the pPXF fit by three times is not sufficient to explain the observed offset of our sample galaxies in the $M_{BH} - \sigma_e$ plot.

The possible reasons for the observed offset are discussed in Section: 5.

5 DISCUSSION

5.1 Possible reasons for the observed offset in the $M - \sigma_e$ plot

It is now well established that BHs and bulges co-evolve (e.g. [Heckman et al. 2004b, Volonteri 2011]), though there are exceptions found in bulgeless galaxies (Seacrest et al. 2013; Simmons et al. 2013). One of the strongest observational indicators for this co-evolution is the $M - \sigma_e$ correlation (Gültekin et al. 2009, McConnell & Ma 2013 and references therein). Using the bulge velocity dispersions, we plotted our galaxies on the BH mass - velocity dispersion ($M - \sigma_e$) correlation (Figure: 8). Most of our sample galaxies ($\sim 80\%$) lie below the correlation.

The observed offset of our sample in the $M - \sigma_e$ plot could be explained due to an over-estimation of $\sigma$ and/or an under-estimation of $M_{BH}$. In this section we describe these possibilities in detail and then explain why we think that the observed offset of our sample galaxies in the $M - \sigma_e$ correlation is real.

5.1.1 Methods adopted for the estimation

Offset in $M_{BH}$: The $M_{BH}$ of three LSB galaxies in our sample, with identification numbers, 1 (1226+0105), 12 (LSBC F727-V01) and 24 (UGC 6614) have been previously estimated by various groups. [Greene & Ho (2007)] estimated the BH masses of galaxies, 1226+0105 and LSBC F727-V01 as $2.51 \times 10^7 M_\odot$ and $0.63 \times 10^7 M_\odot$ respectively. The error bars associated with the $M_{BH}$ estimates are not provided. They used the formalism provided by [Greene & Ho (2003)] for the $M_{BH}$ estimation. Our $M_{BH}$ estimates for 1226+0105 and LSBC F727-V01 are $3.63^{+0.35}_{-0.30} \times 10^7 M_\odot$ and $1.37^{-0.12}_{+0.14} \times 10^7 M_\odot$ respectively and both the values are slightly higher than the estimates of [Greene & Ho (2007)].

Our estimates were obtained using the relation given by [Reines, Greene & Geha (2013)] who have also followed the approach outlined in [Greene & Ho (2002)] to estimate the $M_{BH}$, but with the modified radius-luminosity relationship of [Bentz et al. (2013)]. This modification causes a difference in $M_{BH}$ estimates in these galaxies, of the order of $\sim 1.7 \times 10^7 M_\odot$. The differences between our estimates and that from [Greene & Ho (2007)] are within this range. For UGC 6614 with identification number 24, the $M_{BH}$ estimates are provided by [Naik et al. (2010)] and [Ramya, Prabhu & Das 2011]. [Ramya, Prabhu & Das (2011)] estimated the $M_{BH}$ using the same technique that we used (from the single epoch measurements of Hα emission line from the spectra obtained from Himalayan Chandra Telescope and used the Starburst 99 model to remove the stellar continuum of the host galaxy) and obtained a BH mass of $3.89^{+1.14}_{-1.04} \times 10^6 M_\odot$. From Table 3, we can see that our $M_{BH}$ estimate for UGC 6614 is $4.44^{+0.63}_{-0.58} \times 10^6 M_\odot$ and these two values match well within errors. For all these three galaxies, the $M_{BH}$ estimates from previous studies based on single epoch measurements are in the same order of magnitude with our estimates. Out of these three galaxies the galaxy number 1 lie on the observed $M - \sigma_e$ correlation, whereas the galaxies, 12 and 24 lie below the correlation. The small differences in the estimates are not sufficient to explain the observed offset of these two galaxies. [Naik et al. (2010)] used the technique of excess variance in X-ray emission and determined a mass of of $0.12 \times 10^6 M_\odot$. The estimate of $M_{BH}$ from [Naik et al. (2010)] is lower than our estimate. This can be attributed to the uncertainties in the method adopted. But this order of difference in the mass estimates are also not enough to explain the observed offset in the $M - \sigma_e$ correlation.

In the present work, the virial BH masses of broad line AGN candidates are estimated using the single epoch Hα emission line measurements. The formalism [Reines, Greene & Geha 2013, Greene & Ho 2005]) is based on the strong empirical correlation between the radius of the broad line region and the continuum luminosity and also the scaling relations using the reverberation mapping $M_{BH}$ estimates. The virial BH masses are subject to a number of uncertainties, even the different procedures to measure luminosities and line widths used in the virial mass estimators can cause discrepancies [Shen et al. 2008]. The broad line region geometry varies considerably from object to object [Barth et al. 2011] and assuming a single value for the geometric scaling factor, $\epsilon$ (here we assume a value, $\epsilon = 1$) can cause uncertainties in the $M_{BH}$ estimates. The value of scale factor which is physically associated with the geometry of the broad line region has a range ($\epsilon \sim 0.75-1.4$ Grier et al. 2013) and the geometry varies for each galaxy. If we adopt the values 0.75 and 1.4 then we obtain the lower and upper
The $\sigma$ estimates based on our method for the sample with independent $\sigma$ measurements. The previous estimates of $\sigma$ values of all the galaxies in the table, except NGC 5273 are taken from Grier et al. (2013). For NGC 5273, the $\sigma$ estimates are from Bentz et al. (2014). For NGC 5273 the $\sigma_e$ (74.1 ± 3.7) was provided in (Bentz et al. 2014) and we converted that to $\sigma$ using the effective radius ($r_e = 18.2$) values taken from SDSS database.

| Galaxy     | Previous estimate of $\sigma$ (km/s) | Our estimate $\sigma$ (km/s) |
|------------|--------------------------------------|-------------------------------|
| NGC 5273  | 72.8±3.7                             | 73.3±7.3                      |
| Mrk 202    | 78.0±3.0                             | 83.6±14.6                     |
| Arp 151    | 118.0±4.0                            | 129.8±9.0                     |
| SBS1116+583A | 92.0±4.0                            | 86.0±16.8                     |
| Mrk 590    | 189.0±6.0                            | 196.4±5.8                     |

and the empirical relations provided by Reines, Greene & Geha (2013), between broad Hα luminosity and continuum luminosity, $L_{5100}$, and the FWHM of Hα and Hβ.

$$\log \frac{M_{BH}}{M_\odot} = 7.39 + 0.5 \log \frac{L_{5100}}{10^{44} \text{ ergs s}^{-1}} + 1.09 \log \frac{\text{FWHM}_{H\alpha}}{10^3 \text{ km s}^{-1}}$$

and was used to re-estimate the $M_{BH}$ of our sample. The re-estimated $M_{BH}$ is plotted against $\sigma_e$ and is shown in the lower left panel of Figure: 9. From the plot we can see that the $M_{BH}$ of the sample galaxies have slightly increased and the points have moved closer to the $M_{BH}$ - $\sigma_e$ correlation. But the majority of our sample galaxies are still significantly off from the correlation and hence the systematic bias in the estimation of $M_{BH}$ due to the assumption, $M_{BH} \propto$ (FWHM of Hβ)$^2$ is insufficient to explain the observed offset of our sample from the $M_{BH}$ - $\sigma_e$ correlation.

**Offset in $\sigma$:** Bentz & Katz (2013) have provided a database of AGN BH masses, for a sample of 60 galaxies, estimated using reverberation mapping. From the sample of 60 galaxies we selected the bulge dominated galaxies which have SDSS DR10 spectra and also have BH masses in the range of our estimates ($\sim 10^6 - 10^7 \, M_{Sun}$). We got a sample of 5 galaxies (NGC 5273, Mrk 202, Mrk 590, Arp 151 and SBS1116+583A) which satisfy our selection criteria. For this sample of five galaxies (in Table: 2), independent single epoch velocity dispersion measurements (Mrk 202 and SBS1116+583A have estimates from Keck/ESI observations, Arp 151 has estimates from double spectrograph in Palomar Hale 5 m telescope, Mrk 590 has measurements from 4 m telescope at Kitt Peak National Observatory and NGC 5273 has $\sigma_e$ measurements from the IFU 4.2 William Herschel Telescope) are available. The previous estimates of $\sigma$ values of all these 5 galaxies, except NGC 5273 are given in Grier et al. (2013). For NGC 5273, the $\sigma$ estimate is from Bentz et al. (2014). For NGC 5273 the $\sigma_e$ (74.1 ± 3.7) was provided in Bentz et al. (2014) and we converted that to $\sigma$ using the effective radius ($r_e = 18.2$) values taken from SDSS database. The $\sigma$ values are given in Table: 2. We applied our procedure to estimate the $\sigma$ values to these 5 galaxies and the values are given in Table: 2. The values estimated by us are consistent with the above $\sigma$ values and this suggests that the estimation of $\sigma$ from SDSS matches with the estimates from other observations. It should be noted that all the five galaxies in Table 2 are QSO’s and are dominated by the AGN emission which makes the stellar velocity measurements difficult. The LSB galaxies in our sample are low luminosity AGNs and the SDSS spectra have sufficient S/N to estimate the stellar velocity dispersion. Thus the methodology adopted to compute the $\sigma$ value is appropriate and the uncertainties in the method are not likely to be the reason for the observed offset of our sample in the $M$-$\sigma_e$ correlation.

Recent studies by Bellovary et al. (2014) suggested that line of sight effects due to galaxy orientation can affect the measured $\sigma$. They found that the edge-on orienta-
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Figure 9. The lower left panel shows the $M_{BH} - \sigma_e$ correlation with $M_{BH}$ estimates based on the formalism by (Wang et al. 2009). The lower right panel shows the $M-\sigma_e$ plot with the BH masses estimated using the formalism by (Wang et al. 2009) and with a 20% reduction in the observed $\sigma$ values. The upper left panel shows the $M-\sigma_e$ plot for the BH masses estimated using $\epsilon$ value of 1.4. The upper right panel shows the $M_{BH} - \sigma_e$ plot with 20% reduction in the observed $\sigma$ values. The linear regression lines given by (Tremaine et al. 2002), Ferrarese & Merritt 2000 (G{"u}ltekin et al. 2009), (Kormendy & Ho 2013) relation for the classical bulges/elliptical galaxies and (McConnell & Ma 2013) relation for late type galaxies (dashed, solid, dotted, short-long dashed and long-dashed lines, respectively) for $M_{BH}$ against $\sigma_e$ are also shown in all the panels.

tions give higher velocity dispersion values, due to contamination by non-bulge/disk stars when measuring line of sight quantities. Studies by Hartmann et al. (2014) and Debattista, Kazantzidis & van den Bosch (2013) also suggest that the $\sigma$ measurements can be affected by the contamination of line of sight stars. According to all these studies the disk contamination in highly inclined systems can increase the bulge velocity dispersion up to 25%. The ellipticity (b/a) based on SDSS images of all of our sample galaxies are available in the SDSS database and ranges from 0.54 - 0.95. Ellipticity can be used as a proxy of galaxy inclination and it can be used to correct the observed $\sigma$ for orientation effects. Though Bellovary et al. (2014) find a correlation between the $\sigma$ and galaxy inclination they did not find any trend of
σ with ellipticity. Bellovary et al. (2014) suggested that this may be due to the reason that the ellipticity changes with radius and can be affected by the non-axisymmetric shapes as well as inclination. They recommend to use the kinematic inclination estimates for the correction of orientation effects in the observed σ. Hartmann et al. (2014) found that in barred galaxies, the effect of redistribution of angular momentum due to bars can also cause an increase of σ in the central region (average of 12% increase with a maximum of 20%).

Here we consider the extreme case, of 25% increase of bulge velocity dispersion suggested due to the effect of orientations effect of host galaxy. This in turn suggests that a reduction up to 20% in the observed σ measurements is required to correct the effect of galaxy orientation. We considered this extreme case of reduction of 20% in the σ values of all the galaxies in our sample and re-plotted the M–σ correlation. This is shown in the upper right panel of Figure: 9. The figure shows that though the sample galaxies move close to the M–σ correlation, majority of our sample are still off from the correlation. The identification number of our galaxies are not shown to avoid crowding. They are similar to what is shown in Figure: 8. The plot suggests that the orientation effects of galaxy cannot solely explain the observed offset of all the galaxies in our sample.

Thus the effects which can increase the observed σ, explained above, individually cannot explain the observed offset in σ of all the galaxies in our sample. A detailed study involving observations and simulations of the nature of the different components of these galaxies are necessary to understand the evolution of black holes in LSB galaxies.

Combined offset in M_{BH} and σ: From the above two sub-sections we found that an under-estimation and over-estimation of M_{BH} and σ respectively based on the uncertainties in the methods adopted for their estimation, cannot explain the observed offset of our sample LSB galaxies from the M–σ correlation (upper left, upper right and lower right panels of Figure: 9). At the same time we need to check the combined effect on these galaxies. In the lower right panel of Figure: 9 we plotted the M_{BH} estimates, based on the formalism by Wang et al. (2004), against the σ values which are reduced by 20% (which is an upper limit of the effect on σ due to the orientation of host galaxies). The plot shows that when a combined effect is considered, most of the sample galaxies lie close to the M–σ correlation. But still the offset is present in many of the galaxies. Here we would like to point out that, the reduction in σ considered here is the upper limit of the effect of orientation of the host galaxy to the observed σ. Thus the offset of all our sample from the M–σ correlation may not be explained only by these effects. The intrinsic properties of the LSB galaxies may also contribute to the observed offset. This possibility is explained in the Section: 5.2.

5.2 Is the lack of BH - bulge co-evolution an intrinsic property of LSB galaxies?

A significant fraction of bulge dominated GLSB galaxies have large bulges (Galaz et al. 2006, Morelli et al. 2012) and so it is not surprising that GLSB galaxies show AGN activity, despite having low luminosity disks. However, what is surprising is that most of GLSB bulges appear to host relatively low mass BHs and many not even fall into the SMBH regime (> 10^6 M_☉) (Ramya, Prabhu & Das 2011). The galaxies in our sample have BH mass in the range 10^{-3} – 10^{-2} M_☉ and majority of them lie below the M_{BH} - σ correlation of the elliptical galaxies. The precise M_{BH} estimates for a group of spiral galaxies with maser disks (from megamaser measurements, Kuo et al. 2011) are also ~ 10^7 M_☉. These galaxies also lie below the M_{BH} - σ correlation of massive elliptical galaxies (Greene et al. 2010).

Theoretical models predict a M_{BH} - σ correlation of the form M ∝ σ^α where α = 4 to 5; the value of the constant α depends on whether the early BH mass accretion models included momentum driven winds (Silk & Rees 1998), or thermally driven winds (Fabian 1999). The winds result in shocked shells of matter that are driven outwards and ultimately fragment to form stars that contribute to the growth of the bulge (King & Pounds 2003). In both models mergers play an essential role in driving gas into the nucleus and fueling BH accretion leading to coupled BH-bulge growth. Since mergers are important in the theoretical framework for explaining the M – σ correlation, a possible explanation for some of the galaxies lying below the M – σ correlation (as well as having low mass BHs) could be the lack of major mergers in the history of their evolution. The two reasons supporting this hypothesis are, (i) Most GLSB disks appear relatively undisturbed in appearance; they do not show signs of recent merger event. Although some GLSB galaxies such as UGC 6614 have prominent rings that could be the result of galaxy collisions (e.g. Mapelli & Moore 2008), secular evolution can also result in the formation of such rings (Kormendy & Kennicutt 2004). (ii) They are usually isolated galaxies and often lie close to the edges of voids.

Cisternas et al. (2011) found that triggers for major BH growth since z~1 are not due to major galaxy mergers, but due to alternate mechanisms like internal secular processes and minor interactions. From the study of quasar host galaxies at z~2, Schawinski et al. (2012) found that the predominant driver of massive BH growth in these galaxies are secular processes rather than major mergers. Semi-empirical modelling of AGN fueling by Hopkins, Kocevski & Bundy (2014), suggested that the secular processes dominate the black hole growth in the low mass end. Menci et al. (2014) investigated the effect of disk instabilities in triggering AGN in isolated galaxies and found that it can efficiently provide the BH accretion in the low luminosity end. Kormendy & Ho (2013) and references therein suggest that the local AGNs in late type spirals accrete at sub-Eddington rates and they have low BH masses (10^6 - 10^7 M_☉). These BHs grow mainly by secular processes and they do not co-evolve with their host galaxies. These studies suggest that secular processes dominate the growth of low mass BHs in our sample of LSB galaxies. Secular evolution leads to formation of pseudo bulges in disk galaxies (Kormendy & Kennicutt 2004). Kormendy, Bender & Cornell (2013) did a detailed classification of the bulges in the galaxies for which dynamical BH mass estimations were available and found that the BHs do not co-evolve with pseudo bulges. The majority (7 out of 9) of the maser disk galaxies with low mass BHs are found to have pseudo bulges (Greene et al. 2010). Jiang et al. (2011) did a systematic study of the properties of the 147 active host galaxies with low mass BHs (10^7 - 10^8 M_☉) using HST observations. They found that majority of
the sample galaxies with disks host pseudo bulges and only a small fraction host classical bulges. But interestingly, based on the structural classification by Simard et al. (2011), the majority of our sample LSB galaxies have bulges which are of classical nature (bulge Sersic index $\geq 2.5$, Table 1).

Debattista, Kazantzidis & van den Bosch (2013) suggested that when a disk forms around a pre-existing classical bulge, due to gravitational compression $\sigma_e$ increases. Then an increase of $M_{BH}$ by an average of 50-65% is required to satisfy the M-$\sigma_e$ relation. If there is no corresponding growth in $M_{BH}$, then sample with classical bulges are expected to have an offset. They did not find any such offset in the M-$\sigma_e$ relation of classical bulges in the sample of Guittetin et al. (2009). Based on this they concluded that the BH in the classical bulges was growing along with the disk evolution. They also suggested that growth of BHs might be regulated by the AGN feedback. If the galaxies in our sample which show significant offset have classical bulges in their center, that would suggest that the bulge has not evolved with the disk and lack BH - bulge co-evolution. The structure and kinematics of the BLR, at least as crudely encoded in the $f$ factor, seems to be related to the large-scale properties or formation history of the bulge (Ho & Kim 2014). A detailed study on the classification of the bulges is required to better understand their relation between the observed offset of the LSB galaxies in the $M_{BH}$ - $\sigma_e$ correlation and we plan to do this as a future work.

The secular processes and formation of pseudo bulges are mainly facilitated by bars and by other instabilities like spiral arms in the disk (Kormendy & Kennicutt 2004). In the case of LSB galaxies, which are dark matter dominated even significantly in the inner regions, have featureless disks due to the suppression of disk instabilities by dark matter halos. Thus the formation of bulges and their properties in these systems are hence not clearly understood. The effect of dark matter may increase the potential experienced by stellar population in the bulge and hence increase the $\sigma_e$ values which can lead to the offset of these galaxies in the $M_{BH}$ - $\sigma_e$ correlation. AGN feedback is one of the natural mechanisms for BHs to regulate their growth and to couple with the host galaxy properties. Booth & Schaye (2010) explored the correlation between SMBH mass and the mass of the hosting dark matter halo. From their simulations, they suggested that the mass of SMBH is regulated primarily by the dark matter halo mass and not by the stellar mass of the galaxy. Krumpe et al. (2013) also suggested a positive correlation of dark matter halo mass on the mass of BHs which is prominent in the BHs with $M_{BH} \sim 10^{8-9} M_\odot$. In the case of LSB galaxies, the effect of dark matter in the self regulation of black hole growth through AGN feedback and its coupling with the host galaxy properties may be important and it needs to be analysed further. It is necessary to obtain more direct measures of halo properties, such as halo mass to understand BH growth in LSBs. Another mode of BH growth, which is through disk instabilities can also have an impact in the dark matter dominant LSB galaxies. The low surface gas density in these systems can also affect the growth of BHs and bulges.

5.3 Do LSB nuclei harbor Pristine BHs?

Seed BHs that are formed in the early universe grow by mass accretion to become the massive BHs in galaxies that we observe in our local universe; the accretion is driven by galaxy mergers and interactions. The most massive BH seeds formed from gravitational collapse of large gas clouds whereas the lighter BH seeds formed from the evolution of Population III stars (Volonteri 2010 and references therein). Models predict higher fraction of low mass galaxies to contain nuclear black holes if seeds are created from Population III stars (Volonteri, Lodato & Natarajan 2008). From the study of low mass BHs in small galaxies, Greend 2012 found a tentative evidence that the progenitors of SMBHs were formed via direct collapse rather than from deaths of Population III stars using a simple argument of the occupation fractions, matching with the models of Volonteri, Lodato & Natarajan (2008). The observational evidence for the presence of SMBH ($10^9 - 10^{10} M_\odot$) at early epochs ($z\sim$7-10) poses time constraints on the growth efficiency of their seeds. Giving a jump start to the growth process through more massive seeds ($10^9-10^{10} M_\odot$) and/or occurrence of super Eddington accretion episodes may overcome this limitation. These have been investigated thoroughly by Pacucci, Volonteri & Ferrara (2013) and references therein. They found that the seeds in the mass range ($10^3 - 10^4 M_\odot$) evolve less efficiently and those seeds in the mass range ($10^6 - 10^7 M_\odot$) grow very rapidly. The end product of these massive seeds depends on the initial seed mass, the halo mass and density profile and the accretion scenario (standard Eddington-limited accretion or slim accretion disk appropriate for super Eddington accretion). The spectrum of the emerging radiation, for a massive BH observed at $z=9$, will be dominated in the infrared-submm (1-1000 micron) and X-ray (0.1-100 keV) bands and the future instruments like JWST and ATHENA could detect them (Pacucci et al. 2013, Natarajan 2011), using models of direct collapse, predicted that LSB galaxies and bulgeless galaxies with large disks are less likely to form massive black hole seeds at high redshifts. According to Johnson et al. (2012) extremely massive stars ($\sim 10^5 M_\odot$) at $z \sim 10$ could collapse into BHs which could be the promising seed candidates for the origin of SMBHs (of the order of $10^6$) at $z \sim 7$. The recombination emission from the surrounding H II regions of the super massive stars in the early universe may be bright enough to be detected by future missions such as JWST. Alternatively, BH seeds for IMBHs or SMBHs could be formed from fluctuations in the early Universe during or soon after inflation (Khlopov 2010). Another process for seed BH formation is through the evolution of dark stars. This is very relevant for LSB galaxies because they have a high dark matter content. Unlike regular stars that are supported by fusion, dark stars are supported by the energy released from dark matter particle or WIMP annihilations (Spolyar et al. 2009). Such stars could later evolve into massive BHs in the nuclei of LSB galaxies. Dark stars which have cooler temperatures than the fusion powered stars can accrete baryons all the way up to $\sim 10^5 M_\odot$. The observational signatures and capabilities of future missions like JWST to detect of these dark stars are discussed in literature (Ilie et al. 2012, Rindler-Daller et al. 2013).
Simulations suggest that both gas accretion and galaxy mergers are important for the growth of seed BHs in the centers of galaxies as both processes lead to gas accretion by the nuclear BH (Angles-Alcazar et al. 2013). But at high redshifts the growth is probably driven by gas accretion from the surroundings, resulting in the formation of SMBHs in the centers of massive host galaxies. These SMBHs lie close to the $M - \sigma$ relation. As the gas supply reduces, galaxy mergers and accretion events may play a more important role in BH growth (Dubois, Volonteri & Silk 2014). However, if a galaxy is isolated, the rate of gas accretion maybe too slow and the rate of galaxy mergers too low for the seed BHs to grow beyond $10^6 M_\odot$ at redshift $z=0$. These relatively lighter nuclear BHs in isolated galaxies, can grow through slow accretion leading to relatively low mass BHs ($<10^6 M_\odot$) that lie below the $M - \sigma$ relation (Volonteri & Natarajan 2009). Alternative models have also been proposed for the formation of intermediate mass BHs that have masses less than $<10^6 M_\odot$ (Pacucci & Ferrara 2014).

Bulge dominated LSB galaxies, such as those presented in this study, may be an example of such systems. These low mass BHs are relatively Pristine as they have not undergone as much gas processing as SMBHs in massive galaxies. Thus they can reveal important clues to the initial BH mass function and help us constrain the early evolution of BHs in galaxies. The BH masses in LSB galaxies lie in the $10^6 - 10^7 M_\odot$ range and the majority are outliers on the $M - \sigma$ relation. Also, the Eddington ratios of majority of them are not high (see Table 3). Hence their BHs are not accreting at a high rate and they fall in the low luminosity AGN (LLAGN) class (Nagar, Falcke & Wilson 2003; Heckman et al. 2004a). Thus, the BHs in LSB galaxies represent one of the best candidates for Pristine BHs and a good place to study seed black holes in our local universe. Other low mass BH candidates for such studies are those found in bulgeless galaxies (e.g. Satyapal et al. 2014; Araya Salvo et al. 2012) and dwarf galaxies (Thornton et al. 2008; Reines et al. 2011, Reines, Greene & Geha 2013; Moran et al. 2014).

### 5.4 Nuclear Outflow from AGN in GLSB galaxies

Theoretical models of galaxy formation and evolution often invoke feedback from AGNs and SNe to explain the quenching of star formation in galaxies and hence formation of very massive galaxies in the universe (Di Matteo, Springel & Hernquist 2003). Outflows are believed to be one of the signatures of AGN feedback and hence forms an important evidence to test the BH-bulge co-evolution. Numerical simulations indicate that feedback is triggered during an intense and rapidly accelerated BH fueling phase during a gas-rich galaxy merger (Narayan et al. 2010 and references therein). So one would expect to see extreme outflowing gas moving with velocities greater than 1500 km s$^{-1}$ only in a high-z quasar or/and ULIRGs associated with AGNs accreting at high eddington ratios.

Interestingly, a few galaxies in our sample show signatures of outflows. The three galaxies in our sample, UGC 6614 (identification no 24), UGC 6284 (identification no 28) and UGC 5035 (identification no 30), which are classified to be LINERs show blue-shifted component in Hα emission lines. For UGC 6614, along with the blue shifted outflow component, there is a broad component which is associated with the BH accretion. The blue shifted Hα component in these galaxies suggest the presence of an ionised gas outflow. The forbidden [O iii] emission lines are ideal tracers of extended ionized outflowing gas which cannot be produced by the high density broad line regions (Cresci et al. 2015). Thus the asymmetric extended [O iii] line profiles are considered as powerful signatures of the presence of outflowing gas. Extended [O iii] emission from quasars are ubiquitously found by many authors (Nesvadba et al. 2008; Greene et al. 2014, Ramya et al. in preparation and references therein). UGC 6614 and UGC 6284 show the presence of outflow components in [O iii] emission line region along with Hα region. This suggests that outflow signatures in these galaxies are real. Whereas, UGC 5035 does not show any outflow signature in the [O iii] region. Thus the blue shifted Hα component in this galaxy may not be associated with any outflow event and may be associated with the broad line region and BH accretion. Along with UGC 6614 and UGC 6284, another four galaxies in our sample, 2MASX J12291286+0049042 (identification no 1), VIII ZW 318 (identification no 2), NGC 7589 (identification no 5) and 2MASX J00534265-0105066 (identification no 7) also show blue shifted outflow signatures in [O iii]. These four galaxies are classified as Seyfert galaxies in the BPT diagrams. The velocity of outflowing gas, $v_{out}$ associated with the [O iii] blue shifted components of the galaxies in our sample are given in Table 3. The emission line fits, similar to Figure 2, of the galaxies which show signatures of outflow are shown in different panels of Figure: 10.

UGC 6614 shows outflow feature in Ha, [O iii] and Hβ regions. The measured Eddington ratio and BH mass for UGC 6614 are 0.024 and $4.44 \times 10^6 M_\odot$ respectively. The outflow component as measured by the blue shifted Ha line is moving at $3064.77 \pm 86.39$ kms$^{-1}$ with a FWHM of 3213 $\pm$ 200 kms$^{-1}$. Similarly the outflow component as measured by Hβ line is moving at $4149 \pm 267$ kms$^{-1}$ with a FWHM of 3304 $\pm$ 667 kms$^{-1}$. The velocity offset and FWHM values of Ha and Hβ components are similar. Ramya, Prabhu & Das (2011) had detected outflow components in Ha and Hβ regions. Our values are similar to their estimates. The Hβ luminosity of the outflowing component can be used to estimate the mass of the ionized gas in the outflow. For further discussions on outflows and estimation of outflow rate, we will concentrate on UGC 6614 alone.

It is possible to obtain an order of magnitude estimate for the mass outflow rate assuming that the outflowing gas is moving in a simple bi-conical distribution of uniformly filled outflowing clouds. We also assume that the farther side of the bi-conical outflow is obscured and hence we detect only the blue shifted emission while the red shifted part is obscured in the observed emission lines (Maiolino et al. 2008)}
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The total ionized gas mass can be estimated using H$\beta$ luminosity and assuming electron number density (n$_e$) of 100 cm$^{-3}$. Then,

$$M_{\text{ion}} = 2.82 \times 10^6 \left( \frac{L_{H\beta}}{10^4 \text{ ergs s}^{-1}} \right) \left( \frac{n_e}{100 \text{ cm}^{-3}} \right)^{-1} \text{M}_\odot$$

The H$\beta$ luminosity of the outflow component in UGC 6614 is $4.24 \pm 0.06 \times 10^4$ ergs s$^{-1}$. Estimated ionized gas mass is $6.77 \times 10^5 \text{ M}_\odot$. The $v_{\text{out}}$ of [O III]$_{5007}$ component is $\sim 141.4$ km s$^{-1}$. Following Cresci et al. (2015) and assuming the radius at which the outflow is detected to be about $\sim 1-3$ kpc (typical size of NLR), we derive the dynamical time $t \approx R_{\text{out}}/v_{\text{out}}$ to be equal to $\sim 7.14 - 21.43$ Myr. Then, the volume-averaged density is estimated as $\rho_{\text{out}} \approx \frac{M_{\text{out}}}{4\pi R_{\text{out}}^3 v_{\text{out}}}$ where $\Omega$ is the solid angle subtended by the outflow. The mass outflow rate is then:

$$\dot{M}_{\text{out}} \approx \rho_{\text{out}} R_{\text{out}}^2 v_{\text{out}} = 3\nu_{\text{out}} \frac{M_{\text{out}}}{R_{\text{out}}^2}$$

The estimated mass outflow rate is then $0.1-0.28 \text{ M}_\odot \text{ yr}^{-1}$. The above outflow rate is estimated from broad [ O III] lines. If we consider the outflow component using H$\alpha$ and H$\beta$ lines, then we will have another estimate for the mass outflow rate which is $\sim 27$ times more than the one estimated using the [O III] emission. The mass outflow
rate estimated from broad Hα (or Hβ) component is 2.7-7.695 M⊙/yr⁻¹. These are order of magnitude estimates and we caution the reader in using them during specific calculations. Using the narrow line Hα luminosity of UGC 6614, we estimate the SFR in this galaxy to be equal to 0.04 M⊙/yr⁻¹. The mass outflow rate is an order of magnitude greater than the SFR in this galaxy and hence clearly indicating that the outflows are powered by the AGN. An important question arises regarding the discrepancy of outflow velocities as seen from Balmer lines (∼3800 km/s and FWHM ∼3000 km/s) and the forbidden [O iii] line (∼141 km/s and FWHM ∼1400 km/s). One explanation could be that these outflows are emitted from two different regions, one close to the BLR region or the intermediate line regions (ILR) and the other from the NLR. The deceleration in velocities from ∼1000km/s (in ILR) to a ∼100 km/s (NLR) is consistent with that seen in nearby Seyfert galaxy NGC 4151 (Das et al. 2005, Crenshaw et al. 2015 and references therein). The mass outflow rate of ∼3 M⊙/yr⁻¹ seen in NGC 4151 is similar to the value obtained using the broad balmer lines for UGC 6614 and could produce effective feedback on scales where circumnuclear star formation and bulge growth occur.

While UGC 6614 shows such large outflow velocities, it is not very common in these systems as only 1 out of 30 LSBs with AGN show this feature encouraging our search for such systems. This further calls for detailed study of the geometry and kinematics of UGC6614 using existing IFUs. Mapelli & Moore (2008) suggest that the progenitors for GLSB galaxies such as UGC 6614, Malin1, Malin2 and NGC 7589 are ring galaxies which is created after an interaction. The gas and stars are redistributed in such an encounter and hence the formation of large diffuse stellar disks. This encounter triggers an AGN which could further create such ionized gas outflows.

The effect of this outflowing gas on the host galaxy is difficult to determine with existing data. Cresci et al. (2013) using VLT SINFONI observations found that the fast expanding outflowing gas sweeps away expelling most of the gas thereby quenching star forming activity along its route, while the outflowing gas also triggered star formation by compression of gas clouds by the outflow-driven shock at the outflow edges. This was a classical case of both positive and negative feedback by fast moving outflows. In UGC 6614 and other LSB galaxies which show signature of outflow, the action of such feedback on the host galaxy can be understood using future IFU observations.

6 CONCLUSIONS

- From the analysis of the SDSS optical spectra of 24 LSB galaxies, We derived the virial mass of their central BHs. The median value of M BH is 5.62 × 10⁶ M⊙.
- Majority of our sample lie below the M BH - σ correlate of the normal spiral galaxies.
- The effects of systematic bias in the M BH estimation and the effect of orientation of the host galaxies in the measurement of σ are insufficient to explain the observed offset of our sample galaxies in the M BH - σ correlate.
- In general, the LSB galaxies tend to have low mass BHs which probably are not in co-evolution with the host galaxy bulges. The isolated and poorly evolved LSB galaxies are good candidates to understand the evolution of heavy seed BHs.
- The lack of bulge - BH co-evolution, indicative of secular evolution in these systems, can be one of the probable reasons for the observed offset. But majority of the LSB galaxies in the sample are likely to host classical bulges (Sersic index ≥ 2.5) which are products of major mergers. A detailed study of the nature of the bulges and the role of dark matter in the growth of the BHs is important and planned to be addressed in future.

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Figure A1. Same as in Figure 2 for other sample galaxies.
Figure A1. Continued
Investigating AGN Black Hole Masses and the $M-\sigma_e$ relation for Low Surface Brightness Galaxies

Figure A1. Continued
Table A1. Fluxes of narrow emission lines in the units of $10^{-17}$ ergs/s/cm$^2$

| Galaxy | $H_\beta$ narrow | [O iii] | [O ii] | [O i] | [N ii] | [N ii] | $H_\alpha$ narrow | [Si] | [Si] |
|--------|------------------|--------|--------|--------|--------|--------|------------------|------|------|
| 4861   | 23.68 ± 0.01     | 0.198  | 9.51 ± 0.5 | 0.77 ± 0.35 | 36.38 ± 1.92 | 107.31 ± 1.92 | 100.94 ± 5.69 | 20.85 ± 4.52 | 24.08 ± 3.91 |
| 4960   | 36.59 ± 3.66     | 107.69 ± 3.66 | 180.43 ± 16.76 | 391.04 ± 6.78 | 300.47 ± 5.63 |
| 5007   | 108.14 ± 9.03    | 36.97 ± 4.51 | 147.27 ± 12.00 | 67.62 ± 9.25 | 46.79 ± 7.70 |
| 6300   | 59.92 ± 3.35     | 14.02 ± 4.69 | 10.05 ± 3.97 | 28.24 ± 1.97 | 83.29 ± 1.97 | 63.19 ± 6.34 | 36.42 ± 4.52 | 35.64 ± 3.63 |
| 6304   | 23.68 ± 0.01     | 0.198  | 9.51 ± 0.35 | 36.38 ± 1.92 | 107.31 ± 1.92 | 100.94 ± 5.69 | 20.85 ± 4.52 | 24.08 ± 3.91 |
| 6548   | 36.59 ± 3.66     | 107.69 ± 3.66 | 180.43 ± 16.76 | 391.04 ± 6.78 | 300.47 ± 5.63 |
| 6584   | 108.14 ± 9.03    | 36.97 ± 4.51 | 147.27 ± 12.00 | 67.62 ± 9.25 | 46.79 ± 7.70 |
| 6563   | 59.92 ± 3.35     | 14.02 ± 4.69 | 10.05 ± 3.97 | 28.24 ± 1.97 | 83.29 ± 1.97 | 63.19 ± 6.34 | 36.42 ± 4.52 | 35.64 ± 3.63 |
| 6717   | 23.68 ± 0.01     | 0.198  | 9.51 ± 0.35 | 36.38 ± 1.92 | 107.31 ± 1.92 | 100.94 ± 5.69 | 20.85 ± 4.52 | 24.08 ± 3.91 |
| 6731   | 36.59 ± 3.66     | 107.69 ± 3.66 | 180.43 ± 16.76 | 391.04 ± 6.78 | 300.47 ± 5.63 |

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Table A2. Estimates of different parameters of galaxies with broad balmer lines.

| Galaxy | \(H_\beta\) \(x 10^{-17}\) erg s/cm\(^2\) | \(H_\alpha\) \(x 10^{-17}\) erg s/cm\(^2\) | FWHM km/s | \(M_{BH}\) \(x 10^6 M_\odot\) | \(\sigma\) km/s | Eddington | \(L_{H_\alpha}\) \(x 10^{40}\) erg/s | \(L_{H_\beta}\) \(x 10^{40}\) erg/s |
|--------|---------------------------------|---------------------------------|------------|-----------------|-------------|-------------|-----------------|-----------------|
| 1      | 332.46±16.82                   | 1463.00±40.39                  | 4453.21±76.08 | 36.30±4.04      | 152.78±7.40 | 0.014       | 18.32±0.51      | 4.16±0.21       |
| 2      | 988.09±36.89                   | 1713.59±35.03                  | 1377.11±79.68 | 6.07±3.53       | 267.89±8.25 | 0.038       | 1.79±0.94       | -               |
| 3      | 130.81±68.33                   | 108.26±26.29                   | 1309.87±36.71 | 0.54±0.32       | 131.09±7.70 | 0.11        | 0.38±0.14       | -               |
| 4      | 116.11±54.55                   | 1172.08±31.59                  | 3758.59±111.36 | 9.44±1.24      | 116.74±4.93 | 0.015       | 2.19±0.10       | -               |
| 5      | 766.36±52.06                   | 5725.13±506.28                 | 2902.42±108.41 | 6.87±0.92      | 148.56±3.85 | 0.08        | 3.46±0.24       | -               |
| 6      | 138.01±22.08                   | 4058.77±374.01                 | 8.67±2.07    | 177.86±4.37    | 0.032       | 1.31±0.21  | -               | -               |
| 7      | 66.81±22.90                    | 1606.80±394.84                 | 2642.06±262.85 | 3.39±0.87      | 212.05±5.13 | 0.072       | 1.17±0.23       | 0.39±0.07       |
| 8      | 115.74±21.77                   | 344.50±69.27                   | 2622.93±192.81 | 3.63±0.81      | 190.43±9.44 | 0.071       | 2.81±0.51       | 0.79±0.18       |
| 9      | 394.75±14.99                   | 776.36±562.99                  | 4745.67±583.01 | 5.70±1.72      | 164.18±4.49 | 0.01        | 0.53±0.12       | -               |
| 10     | 57.58±13.07                    | 204.41±36.83                   | 278.50±24.65 | 586.40±363.53  | 150.79±5.04 | 0.003       | 2.68±0.24       | -               |
| 11     | 174.03±30.51                   | 4815.98±550.28                 | 4172.43±117.01 | 17.46±6.17    | 234.30±3.52 | 0.003       | 0.17±0.03       | -               |
| 12     | 217.72±51.11                   | 4643.30±727.45                 | 221.24±44.97 | 763.90±111.01  | 197.54±7.99 | 0.0004      | 0.36±0.07       | -               |
| 13     | 278.50±24.65                   | 586.40±363.53                  | 227.50±24.65 | 586.40±363.53  | 150.79±5.04 | 0.003       | 2.68±0.24       | -               |
| 14     | 328.33±59.00                   | 6719.39±805.62                 | 17.52±5.18  | 179.99±3.27    | 0.003       | 0.64±0.12  | -               | -               |
| 15     | 267.37±84.94                   | 2887.53 ±469.04                | 17.19±5.13  | 185.77±3.66    | 0.135       | 0.47±0.15  | -               | -               |
| 16     | 92.52±18.56                    | 4497.51±646.77                 | 17.19±5.13  | 185.77±3.66    | 0.135       | 0.47±0.15  | -               | -               |
| 17     | 168.01±54.94                   | 2306.66±303.52                 | 205.73±3.78 | 0.008         | 0.81±0.19  | 0.35±0.07  | -               | -               |
| 18     | 451.72±36.94                   | 2826.95±159.69                 | 4.44±0.88  | 136.46±3.86    | 0.024       | 2.72±0.15  | 0.43±0.04       | -               |
| 19     | 306.51±96.78                   | 6526.04±356.49                 | 17.90±5.50  | 169.40±4.70    | 0.004       | 0.77±0.24  | -               | -               |