Optimization of MBR hydrodynamics for cake layer fouling control through CFD simulation and RSM design

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Abstract

Membrane fouling is an important issue for membrane bioreactor (MBR) operation. This paper aims at the investigation and the controlling of reversible membrane fouling due to cake layer formation and foulants deposition by optimizing MBR hydrodynamics through the combination of computational fluid dynamics (CFD) and design of experiment (DOE). The model was validated by comparing simulations with measurements of liquid velocity and dissolved oxygen (DO) concentration in a lab-scale submerged MBR. The results demonstrated that the sludge concentration is the most influencing for responses including shear stress, particle deposition propensity (PDP), sludge viscosity and strain rate. A medium sludge concentration of 8820 mg L\textsuperscript{-1} is optimal for the reduction of reversible membrane fouling. The bubble diameter is more decisive than air flowrate for membrane shear stress due to its role in sludge viscosity. The optimal bubble diameter was at around 4.8 mm for both of shear stress and PDP.

1. Introduction

Membrane bioreactor (MBR) is an attractive process in space limited areas by replacing the secondary sediment tank for the purpose of separation of water and biomass in wastewater treatment due to its small footprint (Judd, 2011). However, membrane fouling, as the most challenging issue in MBR application, needs
physical and (or) chemical cleaning when it comes to a critical point (Chen et al., 2016; Wang et al., 2014). Nevertheless, it is possible to control fouling before its occurrence. Membrane foulants can be divided into three fractions considering particle diameter as bio-solids, colloids, and dissolved solutes (Wang et al., 2014). The solutes and colloids adsorb to membrane surface and pores, and this fouling is regarded as irreversible and generally removed by chemical cleaning. The bio-solids (microbial aggregates, flocs) deposit on the membranes and often accumulate to compact ‘cake layer’ which is considered as the main cause of fouling problems (Wang et al., 2014). The main factors for MBR membrane fouling control can be separated into four categories as widely reported (Lin et al., 2014; Shen et al., 2015; Yu et al., 2014) as following: activated sludge conditions (including MLSS, particle diameter, viscosity, rheology, SMP, EPS, F/M, surface tensions, zeta potential), operations (bubble diameter, aeration, HRT, SRT, flux, addition of powdered activated carbon or flocculants), configuration (membrane module, reactor) and membrane materials (hydrophobicity, hydrophilicity, membrane structure). Obviously, hydrodynamics has a strong interaction with each one of the above four aspects. The measures to limit sludge cake fouling include the operation under sub-critical flux, the improvement of hydrodynamic conditions, the implementation of intermittent filtration, the addition of flocculants, the selection of proper sludge retention time (SRT), and hydraulic retention time (HRT) (Wang and Wu, 2009). It is well known that hydrodynamics plays the key role in the reversible fouling control such as detachment of cake layer and bio-solids migration (Wang and Wu, 2009). It is clear now that one cure for membrane fouling can be the systematical analysis of effect of hydrodynamics on reversible fouling. In general, shear force is the main consideration for the deprivation of cake layer. As a result, most numerical studies pursued high shear stress through operations such as the increase of aeration intensity and the change of bubble diameter (Böhm et al., 2013). However, the diffusion generated force is more decisive than shear force for the back transportation of bio-solids and cake layer (Drews et al., 2010; Judd, 2011). The parameters influencing particle diffusion and the corresponding optimization were not critically considered. The particle size, for instance, which has limited contribution to the shear stress but is decisive for the bio-solids deposition through diffusion, is often ignored (Amini et al., 2013). This can be a reason why the controversial findings about the particle size related operations on membrane filtration were found (Rosenberger et al., 2005). Meng (Meng et al., 2006) suggested that particle size distribution (PSD) should be taken as a separate membrane fouling factor due to its small correlation with EPS in most MBR operations though some researches showed that particle size may be impacted by the amounts and components of EPS (Wilén et al., 2003). The biomass concentration in the bulk and in the cake layer should also be reconsidered due to its role in both of shear stress and particle diffusion. MLSS concentration can be negative or positive or no impact on membrane fouling as reported (Rosenberger et al., 2005). Schwarz (Schwarz et al., 2006) summarized that increasing MLSS decreased the critical permeate flux, but the effect was strong only for MLSS <5 g L⁻¹. For the typical MLSS zone (>5 g L⁻¹), flux-management techniques to prevent serious cake formation were more important than MLSS. Same situations were found for bubble size. The increase of bubble size can be negative (Drews et al., 2010) or positive (Böhm et al., 2013) on membrane filtration resistance. While some others reported that there was a plateau region of shear stress with the increase of bubble diameter (Amini et al., 2013). To resolve such paradox for MBR operations, the operations related to hydrodynamics for membrane fouling control should be re-examined by introducing more factors affecting hydrodynamics and the physical effects of these parameters need to be separated from biological ones (EPS, SMP). Hydrodynamics evaluation then can be a supplement for the analysis of biological fouling caused by solutes and collides. Jiang (Jiang et al., 2007) set an example to make the controversies explicit. In his study, the submicron particle deposition in a side-stream membrane bioreactor was controlled to some extent through the modification of five variables related to hydrodynamics, i.e., cross flow velocity, membrane tube diameter, membrane length, dry solid contents and temperature while considering the PSD and sludge viscosity. Amini (Amini et al., 2013) introduced a CFD model to study the effect of operations including MLSS concentration and bubble diameter on the membrane shear stress of a full-scale MBR. They found that higher MLSS was preferred for membrane scouring and the optimized bubble diameter was 3 mm within the restrained range of 2 mm–5 mm irrespective of the MLSS concentration. However, the sludge was treated as Newtonian fluid in these studies and the interrelated relationship of different operations was ignored, which left the conclusions of these studies in dispute. Besides, the key control parameter such as dissolved oxygen (DO) was not considered and thus makes these researches far from practical guidance. The hydrodynamics of particle deposition is very complex involving mass and momentum balances, multiphase interaction and species transportation (ANSYS, 2014). More specifically, particle back transporting, membrane scouring and DO concentration can be affected by temperature, airflow rate and mode, bubble shape and diameter, biomass concentration and PSD. This study therefore highlights the comprehensive evaluation and optimization of hydrodynamics on reversible fouling considering sludge conditions (PSD, MLSS and sludge rheology), operations (bubble diameter and aeration intensity) and DO concentration in a lab-scale flat sheet MBR through CFD simulation. It has to be pointed out that it is the thermodynamic forces (interactions between membrane and flocs) that bind (adhere) flocs to the membrane after the flocs move close to the membrane surface by hydrodynamic forces (Lin et al., 2014). Such thermodynamic forces can be described by the extended Derjaguin-Laudau-Verwey-Overbeek (XDLVO) theory which presumes that the total interaction is the sum of attractive Lifshitz–Van der Waals, repulsive electrostatic double layer and acid–base interaction. These three thermodynamic interactions between membrane surface and foulants are functions of their separation distance and surface properties. The XDLVO forces can be affected by many factors such as solution pH, solution ionic strength, surface properties, fractal dimension and floc size etc, and play decisive roles in the final adhesion of sludge foulants (Hong et al., 2014; Lin et al., 2014). However, they are not considered in this study due to its distraction from the focus of this study and the impossibility to acquire the sufficient Nano-level resolution with a CFD modeling of a macro-scale. The traditional one-by-one optimization is time consuming and implicit, and brings misleading results by neglecting the interactions between the input parameters. An expedite methodology is of great needs to evaluate the responses including particle back transporting and membrane scouring in a straightforward manner. The design of experiments approach allows understanding the main interactions between the input parameters and successfully targeting the best operating conditions of MBR with a minimum number of runs. The objectives of this paper are thus (1) to investigate the mechanism and effect of MLSS, bubble diameter, aeration on reversible fouling such as cake layer on the membrane of MBR with the CFD simulation and DOE design, and (2) to obtain the cost-effective control of membrane reversible fouling targeting different responses from the hydrodynamic and practical prospective. Responses of wall shear stress and probability of particle deposition (PDF) under a restrained DO concentration are studied, and the optimal operations of the MBR in favor of one of or both of the two responses are determined.
2. Material and methods

2.1. Experimental setup

A bench-scale submerged flat sheet MBR with a work volume of 60.0 L was used (Fig. 1). Five flat membrane sheets (0.07 m² per sheet, effective filtration area 0.05 m² for each membrane side) (SINAP membrane tech Co., Ltd., China) with a design flux of 20.0 L m⁻² h⁻¹ were packed in the membrane module settled in the geometrical middle of the reactor. The two sides of each membrane sheet were named in forms of ‘mᵢᵃ’ and ‘mᵢᵇ’, where ‘ᵢ’ was the membrane series number along y direction, and ‘ᵃ’ and ‘ᵇ’ indicated the front and back of each membrane sheet, respectively. Three aeration blowers were perpendicular to the membrane surfaces. To generate different bubble size, different groups of blowers with different air-blower orifices’ diameter were prepared.

Hexahedral mesh was generated by using ICEM 15.0 (ANSYS, USA). Local meshes near wall and air-blower orifices were refined and mesh size increased with a growth rate of 1.2 to improve the numerical stability. More layers of meshes were inflated near membrane surface to improve the numerical resolution of these areas. After the grid independent test, the optimized grid used in this work was around 720,000 elements with the maximum and minimum element sizes of 10.0 mm and 0.5 mm, respectively. All the simulations were carried out in FLUENT® 15.0 (ANSYS, USA) on a work station (Thinkstation D30, LENOVO, China) with a 64 bit processor (Intel® Core® 12 Xeon CPU E5649) and 24 GB of random access memory, running at a clock speed of 2.53 GHz.

2.2. Design of experiments of the membrane filtration process

The requirement of a large number of experiments can be very time consuming. Besides, traditional one-by-one experimental optimization is implicit and leads to misleading results by neglecting the interactions between the input parameters. To make the conclusion explicit, the CFD simulations were carried out with the design of experiments approach. The central composite (CCD) approach was applied as the response surface methodology (Silva and Rouboa, 2015). CCD approach allows the understanding the main interactions between the input parameters and successfully targeting the best operating conditions with a minimum number of CFD simulations. The operating conditions of MLSS, airflow rate and bubble diameter in the MBR were chosen due to the remarkable effect on membrane fouling control (Tijing et al., 2015; Wibisono et al., 2014). The ranges of the operations were determined according to the practical MBR operation (Table 1).

2.3. Sampling and analysis

Rheology of activated sludge samples from the MBR was measured by a Haake RS6000 Rheometer® (Thermo Scientific, USA). The measurements were performed in triplicate at shear rates ranging from 0 to 500 s⁻¹. The measuring protocol in detail is referenced to previous work (Yang et al., 2016). The non-Newtonian relationships between shear stress and shear rate were fitted to the yield-pseudo plastic type Sisko rheology model using Matlab® (Mathworks, Inc.). Different biomass concentrations were acquired by diluting or concentrating the sludge adopted from the lab-scale MBR rather than by adjusting the F/M or SRT. PSD of sludge was measured by Malvern particle size analyzer (Mastersizer 2000, England). Activated sludge samples were taken from a steadily operated MBR with a SRT of 20 d for SOUR measuring. The oxygen concentration of the sludge samples was automatically recorded by the fluorescence DO meter (Multi 3410, WTW Co Ltd, Germany) every 10 seconds. The overall volumetric respiration rate (OUR) was calculated from the decreasing concentration of oxygen in the respirometric cell between aeration phases. After that, the sludge was taken out for the measurements of MLSS (mixed liquor suspended solid) and MLVSS (mixed liquor volatile suspended solid) concentrations.

DO concentrations at points of S1 (25 mm, 175 mm, 25 mm), S2 (175 mm, 100 mm, 750 mm), S3 (325 mm, 25 mm, 500 mm) were measured with a fluorescence DO meter (Multi 3410, WTW Co Ltd, Germany) (Fig. 1). The average value of these three DO concentrations was obtained and compared to that of the CFD modeling.

PIV (EM3-03M1500, Microvec Pte. Co., LTD, China) was adopted for the water velocity measurement. Pure water velocity measurements were firstly carried out in the MBR at an airflow rate of 1.0 m³/h. Carboxymethyl cellulose (CMC) and xanthan were then used to replace activated sludge as a rheological fluid for velocity

Fig. 1. Airlift membrane bioreactor in 3D view and its configuration parameters in orthographic views.
measurements with PIV system due to their transparency and pseudo plastic fluids behavior which is similar to the activated sludge (Böhm and Kraume, 2015; Ratkovich et al., 2010). A concentration of 0.5% w/w was used to represent the sludge concentration of around 12.0 g L\(^{-1}\) (Dumont et al., 2002). Water velocities outside the membrane module (L1 and L2) were recorded (Fig. 1). Testing procedures of PIV can be found in the previous work (Yang et al., 2016).

### 3. Model development

#### 3.1. Governing equations of gas–liquid flow

The three-dimensional two-phase mass and momentum conservation equations are solved by the pressure-based solver where the pressure field is shared by the different phases. Each phase is governed by respective mass and momentum conservation equations within the multiphase framework of Euler-Euler (ANSYS, 2014). The Brownian diffusion model underestimates the particle back transport due to the large particles and at high shear rate conditions (Belfort et al., 1994; Jiang et al., 2007) (Fig. 2).

#### 3.2. Sludge rheology and membrane shear stress

The sludge rheology is a key parameter concerning membrane fouling not only because it has significant impact on flow pattern, but the important role it plays in sludge viscosity and the shear rate (Ratkovich et al., 2013). The viscosity of activated sludge was known to differ with many factors, among of which the biomass concentration (MLSS) was known to be the decisive factor (Moreau et al., 2009). In this study, the impacts of other sludge characteristics, such as EPS, SMP, hydrophobicity-hydrophilicity, bio-polymeric clusters (BPC) which may have important impact on sludge viscosity by changing the conditions (Belfort et al., 1994). The shear-induced hydrodynamic diffusion especially for large particles and at high shear rate conditions (Belfort et al., 1994). The shear-induced diffusion diffuse the particles tend to transport to membrane surface due to the drag force of permeate flow which, however, can be offset mainly by the so called back transport forces including Brownian diffusion, shear-induced diffusion, inertial lift, and inerlial lift, (influencing big particles) (Belfort et al., 1994; Jiang et al., 2007) (Fig. 2).

#### 3.3. Particle back transport velocity

The Brownian diffusion model underestimates the particle back transport velocity especially for large particles and at high shear rate conditions (Belfort et al., 1994). The shear-induced hydrodynamic diffusivity, which occurs because individual particles undergo random displacements from the streamlines in a shear flow as they interact with and tumble over other particles, was a possible resolution to the flux paradox (Davis and Sherwood, 1990). The back transport velocity due to shear-induced diffusion (\(J_\text{s}\)) for a dilute solution (\(\phi_s < 0.1\)) proposed by (Davis and Sherwood, 1990) is as follows

\[
J_s = 0.078 \gamma_w \left( \frac{a^2 \phi_m}{L \phi_b} \right)^{1/3}
\]  

where \(k\) is the Boltzmann constant (1.38 x 10\(^{-23}\) kg m\(^2\)/s\(^2\)), \(T\) is the absolute temperature (K) and \(a\) is the particle radius (m).

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#### Table 1

| Operating conditions | Operating range |
|----------------------|-----------------|
| MLSS (g L\(^{-1}\))  | 6.0–18.0         |
| Air flow rate (m\(^3\) h\(^{-1}\)) | 1.0–2.0 |
| Bubble diameter (mm) | 1.0–5.0          |

The membrane shear stress \(\tau_y\) (Pa) is then calculated by,

\[
\tau_y = \eta \left( \frac{\partial u_i}{\partial x_j} + \frac{\partial u_j}{\partial x_i} \right)
\]  

\[
(\text{3})
\]

### Fig. 2. Forces exerted on particles in an airlift flow membrane filtration process.
The shear-induced hydrodynamic diffusivity is proportional to the power of 2/3 of the particle size multiplied by the shear rate (Eq. (7)), whereas the Brownian diffusivity is independent of shear rate and inversely proportional to particle size (Eq. (4)). As a result, Brownian diffusion is important for submicron particles and low shear rates, whereas it is dominated by shear-induced hydrodynamic diffusion in cross flow filtration involving micron-sized and larger particles.

The shear-induced diffusion proposed by Davis and Sherwood is still underestimated the diffusion in the concentration-polarization boundary layer because the concentration-dependent viscosity employed in their model (Davis and Sherwood, 1990). To compensate this, an inertial lift mechanism was proposed by Belfort and co-workers (Belfort et al., 1994; Drew et al., 1991). Inertial lift arises from nonlinear interactions of a particle with the surrounding flow field under conditions where the Reynolds number based on the particle size is not negligible. It involves a lateral migration of particles, which transports particles away from the membrane. The back transport velocity due to inertial lift ($j_i$) of spherical particles under laminar flow conditions in dilute suspensions, where particle–particle interactions are negligible, can be estimated as follows (Belfort et al., 1994):

$$j_i = 0.036 \frac{\rho_o}{\eta} \frac{a^{2/3}}{\nu_w}$$

(8)

Particle–particle and particle–membrane interactions (including entropy, van der Waals interactions and electrostatic interactions), which may play roles in particle transportation to/from the membrane surface for concentrated solutions of colloidal particles but are insignificant for dilute solutions, are not considered in this study (Bowen and Sharif, 1998; Davis, 1992; Elimelech et al., 2013).

For the lab scale MBR in this study, an average back-transport flux at a typical operation, e.g. MLSS concentration of around 150 sL (Fig. 3). It is reported that their reduction can hardly be improved by hydrodynamic approaches (Belfort et al., 1994). While for particles with a diameter larger than 100.0 μm, either shear deved velocity or inertial velocity can overcome the suction force (Jiang et al., 2007). Particles with the diameter between 1.0 μm to 100.0 are more sensitive to hydrodynamics and their transportations are dominantly controlled by shear induced force (Fig. 3).

3.4. Oxygen biotransformation

The DO concentration is expected to vary with the MBR operations. To coordinate the DO concentration and membrane scouring at a cost-effective way, the DO concentration is regarded as a restrictive factor in CFD simulation. The oxygen biotransformation considering biomass concentration, aeration intensity and bubble diameter is thus incorporated into the CFD model. The evolvement of DO in bioreactor is a result of balancing of oxygen transfer from gas to bulking liquid and oxygen consumption by microbial community. They are determined as follows.

1. **Oxygen mass transfer**

   The oxygen mass transfer rate (OTR) is estimated by (Pittoors et al., 2014)

   $$\text{OTR} = k_La(2S_0 - S_b)$$

   (9)

   where $k_La$ (s⁻¹) is the mass transfer coefficient estimated by Eq. (10); $a$ is the oxygen saturation concentration ratio of wastewater to clean water (Tchobanoglous et al., 2002), $S_0$ (mg L⁻¹) and $S_b$ (mg L⁻¹) are the dissolved oxygen saturation concentration of clean water and dissolved oxygen in the liquid phase.

   The $k_La$ takes the form of (Cockx et al., 2001),

   $$k_La = \beta \frac{12\alpha_b}{d_b} \sqrt{\frac{D_b}{\pi d_b}}$$

   (10)

   where $\beta$ is the coefficient considering the effect of wastewater property and sludge concentration, $\alpha_b$ is the gas volume fraction, $d_b$ (m) is the Sauter mean diameter of the bubbles, $D_b$ (m² s⁻¹) is diffusivity of oxygen in the liquid phase, and $\Delta U$ (m/s) is the slip velocity between bubbles and bulking liquid.

2. **Dissolved oxygen consumption**

   The oxygen uptake rate (OUR) is simplified as

   $$\text{OUR} = \text{SOUR}\times\text{MLVSS}$$

   (11)

   where SOUR (h⁻¹) is the specific oxygen uptake rate in the MBR tank, MLVSS (mg L⁻¹) is the mixed liquor volatile suspended solid.

4. Results and discussion

4.1. Model validation

The model simulation was compared to experimental data measured in a lab-scale MBR. For hydrodynamics validation, liquid velocities in pure water and CMC solution (0.5% w/w) were measured, respectively. For species validation, DO concentration was measured in the MBR under 6 conditions of the 15 cases (Table 2). Liquid velocity at $L_1$ and $L_2$ was obtained by the PIV measurements and by the CFD simulation, respectively (Fig. S2). All relative errors were less than 5% suggesting that the model provided an excellent description of flow behavior and DO concentration distribution.

4.2. Particle size distribution and sludge viscosity

The particle size of MBR sludge varies with operations such as SRT (Hocaoglu et al., 2011), HRT (Meng et al., 2007), practical shear...
stress intensity (Stricot et al., 2010), floculants addition (Liu et al., 2015) and influent characteristics (Hao et al., 2016). The particle size distribution of the MBR in this study showed a main peak around 112 ± 10 μm and a long tail between 1 and 10 μm (Fig. S4) which is consistent to the publications which had similar work conditions to this study (Massé et al., 2006; Stricot et al., 2010). The rate at which particles are carried to the membrane surface due to the permeate flow can be balanced by back-transport forces for particles with diameter larger than 100 μm (Fig. 3). The smaller sludge (1–10 μm) are more inclined to deposit due to the weak back transport velocity induced by all the three diffusions. These fine particles along with the soluble foulants (EPS/SMP) will quickly form a thin film and lead to a dramatic drop of permeate flux for the newly installed membranes or membranes after chemical cleaning. Given a critical flux, the critical size of particle deposition, xc can be determined by Eq. (4) to Eq. (8). Then the total volume of particles deposited on membrane or the particles deposition propensity (PDP) can be calculated by,

\[ PDP = w_x \phi_b = \sum_{i=0}^{2} V_i \phi_{b,i} \]  

where \( w_x \) (%) is the percentage of deposited particles, \( V_i \) is the particle volume fraction, \( \phi_{b,i} \) (mg L\(^{-1}\)) is the biomass concentration of the bulk.

The impact of sludge viscosity on membrane scouring is two sides. The shear stress may get down at high sludge viscosity retarding the flow thus making lower shear rate on membrane, but on the other hand the shear stress may go up if the increase of sludge viscosity offsets the decrease of shear rate according to Eq. (3). Operating conditions such as aeration intensity and temperature and configuration of the MBR will impact sludge viscosity even at the same sludge concentration, which can partly explain the discrepancy of the impact of MLSS concentration on membrane filtration (Rosenberger et al., 2002; Stricot et al., 2010). At the same time, the sludge viscosity has an effect on strain rate and thus affects the particle deposition (Eq. (8) and Eq. (9)). As the most decisive factor for sludge viscosity, MLSS concentration is without doubt one of the major considerations for membrane scouring and particle back transportation.

### 4.3. Single response optimization

Fifteen CFD simulations were carried out by varying input factors of air-flow rate, biomass concentration and bubble diameter in agreement with the design of experiments approach. All the other parameters such as temperature, MBR configuration were kept the same. For each one of the fifteen simulations, a set of responses including shear stress, PDP, strain rate and DO concentration was set. The information of all the responses was extracted and was compiled to be used with a Response Surface Method. Data was fitted by using a second order empirical model implied by Response Surface Method and given by Eq. (13).

\[ y = c_0 + \sum_{i=1}^{3} c_i x_i + \sum_{i=1}^{3} c_{i,j} x_i^2 + \sum_{i=2}^{3} \sum_{j<i}^{2} c_{i,j} x_i x_j \]  

where \( y \) is the response, the \( x_i \) terms are the input factors, the \( c_i \) terms are coefficients. The use of this empirical model allows the determination of the optimal \( x_i \) terms to optimize each one of the studied responses.

The empirical model was validated by using different statistical methods embedded in Design-Expert software (Stat-Ease, Inc, USA) and can be used to navigate within the input parameters boundaries. The most important diagnostic methodology to inspect the effectiveness of the predicted model is the normal probability plot of the internal studentized residuals. It measures the number of standard deviations separating the actual and predicted values. The internal studentized residual, \( r_i \), is the residual divided by the estimated standard deviation of that residual.

\[ r_i = \frac{e_i}{\sigma \sqrt{1 - h_i}} \]  

where \( e_i \) is the difference between actual and predicted values for each point; \( h_i \) is the ith diagonal entry in the hat matrix of the orthogonal projection onto the column space of the design matrix; \( \sigma \) is population standard deviation.

All the models for each one of the responses behave as expected for a normal plot of residuals (Fig. S5). Further analysis was carried out by proceeding to the analysis of variance (ANOVA). The suggested empirical model was used to determine the best operating conditions. The use of replicates was not considered because it made no difference for the same scenario based on CFD simulation. As a consequence, some statistics such as the test on lack of fit and the pure error (Anderson and Whitcomb, 2005) was missing. Despite of these, ANOVA analysis for the model was carried out and the standard statistics for the model are given here (Table 3). The \( p \)-values less than 0.05 indicate model terms are significant and the large \( F \)-values further ensure that the selected empirical models are significant. The \( R^2 \)-Squared value, which measures how well the empirical model fits the CFD numerical simulation, however, increases by adding new terms. To compensate for this drawback, new statistics such as Adjusted \( R^2 \)-Squared and Predicted \( R^2 \)-Squared are also presented. The values of Predicted \( R^2 \)-Squared for all responses are high and are in reasonable agreement with that of the Adjusted \( R^2 \)-Squared (Table 3). The adequate precision measures the signal to noise ratio and a ratio greater than 4 is desirable (Silva and Rouboa, 2015). The ratios higher than 4 for all responses ensures that the model prediction of the responses can be used in the design space. In conclusion, all the statistical measures confirm that the empirical models are suitable for the prediction of the membrane fouling indices based on the CFD simulation. The interpolating polynomial expressed in Eq. (13) provided the optimal values for each one of the responses as well as the corresponding optimal operating conditions (Table 4). The \( F \)-values of MLSS for all responses (except DO concentration) are the largest suggesting that the biomass concentration has the predominant effect over the air-flow rate and the bubble diameter (Fig. 4). Membrane shear stress increased with MLSS within the practical range though higher MLSS restrains the strain rate (Table 4). But high biomass concentration is truly detrimental for particle back transportation by increasing the total number of particles in Eq. (12) and by restraining the strain rate \( \gamma_x \) and
sludge viscosity is much more significant than airflow rate. The significance of operations of air intensity, bubble diameter and MLSS on responses of shear stress, PDP, strain rate, viscosity and DO.

The plot shows a bunch of values where the shear stress is approximately constant. This confirms the slight interrelation between bubble diameter and MLSS, and suggests that a multiple optimization considering shear stress and other responses could be expected. With the DO restraining in 1.00 mg L\(^{-1}\) to 6.00 mg L\(^{-1}\), the maximum value of the shear stress at 3.17 Pa was obtained at airflow rate = 2.00 m\(^3\) h\(^{-1}\) and bubble diameter = 4.83 mm within the range of 1.00–10.00 mm, at which the corresponding DO concentration was 1.37 mg L\(^{-1}\). The optimized bubble size is not consistent with (Böhm et al., 2013) who found that a bubble size larger than the channel depth was always preferred for wall shear stress measured with the electro-diffusion method (EDM). One probable explanation is that the viscosity of electrolyte they used for data recording is comparable to the one of water and \(\frac{\mu}{\rho}\) both in Eq. (4) and in Eq. (7). As a result, PDP increased nearly fivefold when MLSS rise from 6000 mg L\(^{-1}\) to 18,000 mg L\(^{-1}\). Besides, a lower MLSS may be more energy-saving due to lower demand for DO (Table 4). The optimal MLSS concentration was thus the lowest for PDP and strain rate but was highest for membrane shear stress (Table 4). The bubble diameter is unexpected to be more important than airflow rate on shear stress (Fig. 4). This is because the impact of bubble diameter on sludge viscosity is much more significant than airflow rate (Fig. 4). The optimal bubble diameter for PDP and strain rate is found to be the same as expected due to the positive correlation of strain rate and particle back transport velocity. The optimal bubble diameter for shear stress, however, is a little smaller. This can be explained by the slight interrelation between bubble diameter and MLSS on shear stress. While the high airflow rate is favored for the shear stress as expected, the high airflow rate is also preferred for PDP (Table 4). This is because the critical diameter of deposit particles is at about 3–12 \(\mu\)m for the 15 studied tests, the particles tending to deposit is dominated by shear induced diffusion which is positive correlated to flow velocity according to Eq. (7).

A more intuitive observation can be obtained through plotting a 3-D plot with each one of the responses as a function of input factors. The membrane fouling related responses as a function of MLSS and bubble diameter under the medium airflow rate was presented (Fig. 5). The 3-D plots for all the other studied airflow rates are quite similar concerning each one of the studied responses.

Fig. 5a shows that the shear stress increases obviously as a function of the MLSS. The shear stress is up to asymptotic values at the largest MLSS and at the bubble diameter ranging from 3 to 5 mm. The plot shows a bunch of values where the shear stress is approximately constant. This confirms the slight interrelation between bubble diameter and MLSS, and suggests that a multiple optimization considering shear stress and other responses could be expected. With the DO restricting in 1.00 mg L\(^{-1}\) to 6.00 mg L\(^{-1}\), the maximum value of the shear stress at 3.17 Pa was obtained at airflow rate = 2.00 m\(^3\) h\(^{-1}\) and bubble diameter = 4.83 mm within the range of 1.00–10.00 mm, at which the corresponding DO concentration was 1.37 mg L\(^{-1}\). The optimized bubble size is not consistent with (Böhm et al., 2013) who found that a bubble size larger than the channel depth was always preferred for wall shear stress measured with the electro-diffusion method (EDM). One probable explanation is that the viscosity of electrolyte they used for data recording is comparable to the one of water and \(\frac{\mu}{\rho}\) both in Eq. (4) and in Eq. (7). As a result, PDP increased nearly fivefold when MLSS rise from 6000 mg L\(^{-1}\) to 18,000 mg L\(^{-1}\). Besides, a lower MLSS may be more energy-saving due to lower demand for DO (Table 4). The optimal MLSS concentration was thus the lowest for PDP and strain rate but was highest for membrane shear stress (Table 4). The bubble diameter is unexpected to be more important than airflow rate on shear stress (Fig. 4). This is because the impact of bubble diameter on sludge viscosity is much more significant than airflow rate (Fig. 4). The optimal bubble diameter for PDP and strain rate is found to be the same as expected due to the positive correlation of strain rate and particle back transport velocity. The optimal bubble diameter for shear stress, however, is a little smaller. This can be explained by the slight interrelation between bubble diameter and MLSS on shear stress. While the high airflow rate is favored for the shear stress as expected, the high airflow rate is also preferred for PDP (Table 4). This is because the critical diameter of deposit particles is at about 3–12 \(\mu\)m for the 15 studied tests, the particles tending to deposit is dominated by shear induced diffusion which is positive correlated to flow velocity according to Eq. (7).

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than for the particle deposition and membrane gel-like layer formation due to the small particle size (Wibisono et al., 2014). Besides, when considering the particle weighting factor according to the cake filtration mechanism (Kozeny-Carman relationship) (Jiang et al., 2007), the most abundant particles (1.75 μm) can be carried away from the membrane only with a critical flux of 7.13 L m$^{-2}$ h$^{-1}$, which is quite low for a practical micro filtration process. These indicate that biomass concentration should be constrained and operation from biological consideration or flocculants addition should aim at reducing the small particle production and improve their degradation for a minimum PDP (Zhang et al., 2011, 2014).

The strain rate decreases with the increase of MLSS as expected (Fig. 5c). The impacts of airflow rate are as equal as MLSS for strain rate whereas bubble diameter hardly affects (Fig. 4). The MLSS concentration is expected to be high in MBR, therefore, it only can be compensated by a high airflow rate to generate a high strain rate for the purpose of particle back transport. It needs to point out that high biomass concentration in MBR will cause a decrease in sludge size due to the stronger particle–particle friction and collision (Massé et al., 2006). And a high airflow rate may worsen the situation.

DO concentration is also presented in Fig. 5d as a function of the MLSS and bubble diameter at an air flow rate = 1.50 m$^3$ h$^{-1}$. As expected, the DO concentration decreases with the MLSS and increases with bubble diameter. There is a certain proportion of areas where DO concentration is lower than 1.00 mg L$^{-1}$, so the DO concentration needs to be constrained during the responses’ optimization.

4.4. Multiple responses optimization

To alleviate reversible membrane fouling in MBR process, it needs to obtain a larger membrane shear stress for the removal of cake layer and a lower particle deposition propensity at the same time. However, according to the single response analysis, there are some conflicts for these two objectives. For example, the high MLSS is favorable for shear stress but detrimental for PDP. Therefore a multiple responses optimization was carried out to justify these two objectives for a maximum alleviation of rever-

Table 5
Optimal operating conditions and response values considering the maximization of multiple responses.

| Propensity          | Shear stress = PDP | Shear stress > PDP | PDP > Shear stress |
|---------------------|--------------------|--------------------|--------------------|
| Optimal targets     | Shear stress       | Shear stress       | Shear stress       |
| Aeration intensity (m$^3$ h$^{-1}$) | 2.00              | 2.00               | 2.00               |
| Bubble diameter (mm) | 4.86              | 4.84               | 4.88               |
| MLSS (mg L$^{-1}$)   | 15.259            | 18,000             | 8820               |
| Response             | Shear stress (Pa)  | 2.67               | 3.05               | 2.18               |
|                      | PDP (%)            | 3.67e$^{-2}$       | 5.11e$^{-2}$       | 1.49e$^{-2}$       |
|                      | Strain rate (s$^{-1}$) | 130.08            | 115.71             | 161.69             |
|                      | DO (mg L$^{-1}$)   | 1.76               | 1.35               | 2.75               |
| Desirability         | 0.51               | 0.54               | 0.66               |

Fig. 5. Membrane scouring indices of shear stress (a), PDP (b), strain rate (c) and DO (d) as a function of bubble diameter and MLSS.
sible membrane fouling. The optimized operating conditions for the maximization of shear stress and PDP of different propensities with the DO concentration constrain are presented (Table 5). As expected, highest air flow rate and moderate MLSS concentration are optimal for the case where shear stress and PDP are equally weighed. Highest MLSS and air flow rate are preferred when shear stress is biased and the optimal MLSS concentration drop to 8820 mg L$^{-1}$ when PDP is preferred (Table 5). Comparing data from that of in Tables 3 and 4, it can be observed that the optimal bubble diameters fall in 4–5 mm. The reason may be two folds. The membrane shear stress is mainly contributed by liquid phase which is lower for the optimized operating conditions (Fig. 6).

5. Conclusions

A numerical approach combining a 3-D two-phase flow CFD model and Response Surface Methodology was used for reversible membrane fouling control. The significance order of factors are MLSS > bubble diameter > aeration intensity and MLSS > aeration intensity > bubble diameter for shear stress and PDP, respectively. High MLSS is favorable for shear stress but also increases the PDP. With a propensity for PDP and a DO concentration constrain, the optimal operations for reversible membrane fouling control in a lab-scale MBR was airflow rate of 2.0 m$^3$ h$^{-1}$, MLSS of 8820 mg L$^{-1}$ and bubble diameter of 4.88 mm.

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Appendix A. Supplementary data

Supplementary data associated with this article can be found, in the online version, at http://dx.doi.org/10.1016/j.biortech.2016.12.027.

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Fig. 6. Shear stress distribution on and critical particle diameter deposition on membrane surfaces with (A) and (C) for the run of optimized condition (airflow rate = 2.0 m$^3$ h$^{-1}$, MLSS = 8820 mg L$^{-1}$, bubble size = 4.88 mm) and with (B) and (D) for the run of center condition (airflow rate = 1.5 m$^3$ h$^{-1}$, MLSS = 12000.0 mg L$^{-1}$, bubble size = 3.0 mm).
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