The XXL Survey: XXXI. Classification and host galaxy properties of 2.1 GHz ATCA XXL-S radio sources

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ABSTRACT

The classification of the host galaxies of the radio sources in the 25 deg² ultimate XMM extragalactic survey south field (XXL-S) is presented. XXL-S was surveyed at 2.1 GHz with the Australia Telescope Compact Array (ATCA) and is thus far the largest area radio survey conducted down to rms flux densities of \( \sigma \sim 41 \mu Jy \) beam\(^{-1}\). Of the 6287 radio sources in XXL-S, 4758 (75.7%) were cross-matched to an optical counterpart using the likelihood ratio technique. There are 1110 spectroscopic redshifts and 3648 photometric redshifts available for the counterparts, of which 99.4% exist out to \( z \sim 4 \). A number of multiwavelength diagnostics, including X-ray luminosities, mid-infrared colours, spectral energy distribution fits, radio luminosities, and optical emission lines and colours, were used to classify the sources into three types: low-excitation radio galaxies (LERGs), high-excitation radio galaxies (HERGs), and star-forming galaxies (SFGs). The final sample contains 1729 LERGs (36.3%), 1159 radio-loud HERGs (24.4%), 296 radio-quiet HERGs (6.2%), 558 SFGs (11.7%), and 1016 unclassified sources (21.4%). The XXL-S sub-mJy radio source population is composed of \sim 75\% active galactic nuclei and \sim 20\% SFGs down to 0.2 mJy. The host galaxy properties of the HERGs in XXL-S are independent of the HERG selection, but the XXL-S LERG and SFG selection is, due to the low spectral coverage, largely determined by the known properties of those populations. Considering this caveat, the LERGs tend to exist in the most massive galaxies with low star formation rates and redder colours, whereas the HERGs and SFGs exist in galaxies of lower mass, higher star formation rates, and bluer colours. The fraction of blue host galaxies is higher for radio-quiet HERGs than for radio-loud HERGs. LERGs and radio-loud HERGs are found at all radio luminosities, but radio-quiet HERGs tend to be more radio luminous than LERGs at a given redshift. These results are consistent with the emerging picture in which LERGs exist in the most massive quiescent galaxies typically found in clusters with hot X-ray halos and HERGs are associated with ongoing star formation in their host galaxies via the accretion of cold gas.

Key words. galaxies: general – galaxies: evolution – galaxies: active – radio continuum: galaxies – galaxies: statistics – galaxies: stellar content

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1. Introduction

Supermassive black holes (SMBHs) play an important role in galaxy evolution: the masses of SMBHs are correlated with the stellar velocity dispersions of the bulges of their host galaxies (e.g. Magorrian et al. 1998; Gebhardt et al. 2000; Graham 2008), and the growth curve of black holes and that of stellar mass in galaxies have the same shape (Shankar et al. 2009). This indicates that the evolution of galaxies and SMBHs are closely linked. One probable reason for this link is that SMBHs exhibit energetic phenomena, called active galactic nuclei (AGN), which can affect the stellar and gas content of their host galaxies, fundamentally altering their properties. This occurs via ‘feedback’, an outflow from the AGN that heats the interstellar medium, which would otherwise collapse to form stars (Boehringer et al. 1993; Binney & Tabor 1995; Forman et al. 2005; Best
et al. 2006; McNamara & Nulsen 2007; Cattaneo et al. 2009; Fabian 2012). Galaxy formation models that include this extra AGN component are able to more accurately reproduce many observed galaxy properties for $z \lesssim 0.2$, including the optical luminosity function, colours, stellar ages, and morphologies (e.g. Croton et al. 2006; Bower et al. 2006). Therefore, AGN feedback is a crucial component to galaxy evolution models and fundamental to overall galaxy evolution.

Observations of AGN host galaxies have suggested that there are two distinct AGN populations. One population is the classical AGN associated with quasars and radio galaxies, which are well described by the unified AGN model (Antonucci & Miller 1985; Barthel 1989; Urry & Padovani 1995). They exhibit a luminous accretion disk (Shakura & Sunyaev 1973) that produces ionising photons, which generate regions of broad and narrow optical emission lines outside the disk. They also feature X-ray emission, which is generated by inverse Compton scattering, and a dusty torus, which is heated by UV and optical emission from the accretion disk. As a result, the torus re-radiates in the mid-infrared (MIR). If the torus is oriented edge-on relative to the line of sight, the broad-line region is obscured, giving rise to type II AGN (Antonucci 1993). Because these AGN radiate across the electromagnetic spectrum (Ebisu et al. 1994) and their optical spectra exhibit strong high-excitation emission lines (such as [OIII]), they are labelled high-excitation radio galaxies (HERGs).

The second AGN population displays low levels of high-excitation emission lines in their spectra or none at all (Hine & Longair 1979; Laing et al. 1994; Jackson & Rawlings 1997; Best & Heckman 2012). The X-ray emitting corona, optical continuum emission from an accretion disk, and MIR emission from an obscuring torus are absent, and their AGN signatures can only be detected at radio wavelengths (e.g. Hardcastle et al. 2007; Hickox et al. 2009). Accordingly, these sources are called low-excitation radio galaxies (LERGs). The typical host galaxies for LERGs are the most massive quiescent galaxies associated with clusters, while HERGs are hosted by galaxies that have lower mass and higher star formation rates (e.g. Tasse et al. 2008; Smolčić 2009; Best & Heckman 2012; Best et al. 2014).

It has been hypothesised that the two AGN populations exhibit fundamentally different black hole accretion modes that result in two distinct forms of feedback (e.g. Hardcastle et al. 2007). LERGs accrete the hot X-ray emitting phase of the intergalactic medium (IGM) found in clusters, generating radiatively inefficient feedback, whereas HERGs accrete the cold phase of the IGM, allowing for radiatively efficient feedback and associated star formation (Heckman & Best 2014). However, the details of feedback as a function of host galaxy and cosmic time and the precise origin of HERG and LERG differences are poorly understood.

The most direct way to measure the evolution of radio sources is via the construction of the radio luminosity function (RLF). Only a few studies have constructed individual RLFs for HERGs and LERGs (Best & Heckman 2012; Best et al. 2014; Pracy et al. 2016). The results indicate that for $z \lesssim 1$, HERGs evolve strongly and LERGs exhibit space densities that are consistent with weak or no evolution. However, the radio data in these studies probed no deeper than $S_{1.4\,\text{GHz}} \sim 3\,\text{mJy}$ (over very large areas of $\gtrsim 800$ deg$^2$), and so the RLFs are not well constrained at the low-luminosity end ($L_{1.4\,\text{GHz}} \lesssim 10^{22}\,\text{W Hz}^{-1}$). In addition, the HERG and star-forming galaxy (SFG) RLFs from these papers disagree with each other for $L_{1.4\,\text{GHz}} \lesssim 10^{24}\,\text{W Hz}^{-1}$, indicating that these two populations can be difficult to identify at low radio luminosities. On the other hand, Smolčić et al. (2009) studied the evolution of the low-luminosity ($L_{1.4\,\text{GHz}} \lesssim 5 \times 10^{25}\,\text{W Hz}^{-1}$) and high-luminosity ($L_{1.4\,\text{GHz}} \gtrsim 5 \times 10^{25}\,\text{W Hz}^{-1}$) radio AGN down to $S_{1.4\,\text{GHz}} \gtrsim 50\,\mu\text{Jy}$ and out to $z = 1.3$ in the $\sim 2$ deg$^2$ COSMOS field (Schinnerer et al. 2007), but did not distinguish between HERGs and LERGs.

A full understanding of the HERG and LERG luminosity functions, host galaxies, and cosmic evolution is needed in order to understand the physical driver for their differences, and therefore the role of the two different feedback modes in galaxy evolution as a function of time (Best & Heckman 2012 and references therein). Such a precise understanding can test and inform AGN synthesis models, such as that of Merloni & Heinz (2008). Therefore, it is important to identify the HERG and LERG populations across different cosmic epochs so that their impact on galaxy evolution is not conflated. This requires a deep radio survey conducted over a relatively wide area with a large amount of complementary multiwavelength coverage in order to separate between the LERG, HERG, and SFG populations, especially at low radio luminosities. The 2.1 GHz radio survey of the 25 deg$^2$ ultimate XMM-extragalactic survey (Pierre et al. 2016, hereafter XXL Paper I) south field (XXL-S; $\alpha = 23^h30^m00^s$, $\delta = -55^\circ00'00''$, conducted with the Australia Telescope Compact Array (ATCA), is thus far the largest area radio survey conducted down to rms flux densities of $\sigma \sim 41\,\mu\text{Jy}\text{ beam}^{-1}$ (Butler et al. 2017, hereafter XXL Paper XVIII). The excellent multiwavelength coverage of XXL-S allows for the construction of the HERG and LERG RLFs in multiple redshift bins. When completed, they will be the most sophisticated RLFs to date.

First, however, the radio sources must be separated into the AGN and SFG populations. This paper describes the process and results of the classification of the radio sources in XXL-S as LERGs, HERGs, and SFGs. In Section 2, the data, cross-matching procedure, and final sample properties are described. Section 3 details the multiwavelength classification scheme and decision tree used to classify each source. In Section 4, AGN selection effects, possible misclassifications, the distribution of sub-mJy radio sources, and the properties of the host galaxies of LERGs, HERGs, and SFGs are discussed. Section 5 contains the summary and conclusions. Throughout this paper the following cosmology is adopted: $H_0 = 69.32\,\text{km s}^{-1}\,\text{Mpc}^{-1}$, $\Omega_m = 0.287$, and $\Omega_{\Lambda} = 0.713$ (Hinshaw et al. 2013). The following notation for radio spectral index ($\alpha_R$) is used: $S_{\nu} \propto \nu^{\alpha_R}$.

2. Data and sample

2.1. Radio data

The full 25 deg$^2$ of XXL-S was observed with the Australia Telescope Compact Array (ATCA) at 2.1 GHz, with a 2.0 GHz bandwidth, over $\sim 220$ hours on source. The radio data reached a median rms of $\sigma \sim 41\,\mu\text{Jy}\text{ beam}^{-1}$ and a resolution of $\sim 4.8''$. The number of radio sources extracted above 5$\sigma$ is 6287. More details of the observations, data reduction, and source statistics can be found in XXL Paper XVIII.
and Smolčić et al. (2016) (XXL Paper XI). The final source sample in this paper is selected from the radio sources that have reliable optical counterparts (see Section 2.3.2 for the cross-matching method).

### 2.2. Multiwavelength catalogue

There is a wealth of complementary photometric and spectroscopic data available for XXL-S, from X-rays to the mid-infrared, which is contained in a single multiwavelength catalogue. The details of the construction of this catalogue can be found in Fotopoulou et al. (2016) (hereafter XXL Paper VI) and Fotopoulou et al. (in prep.). The following summarises the data available in the multiwavelength catalogue at each wavelength regime.

#### 2.2.1. X-ray data

The XMM-Newton X-ray telescope observed XXL-S as part of the XMM-Newton Extragalactic Legacy survey. The survey achieved a depth of $\sim 5 \times 10^{-15}$ ergs s$^{-1}$ cm$^{-2}$ in the 0.5–2 keV band and $\sim 2 \times 10^{-14}$ erg s$^{-1}$ cm$^{-2}$ in the 2–10 keV band. More details of the X-ray observations, data processing, and simulations can be found in XXL Paper I.

#### 2.2.2. Ultraviolet data

The GALEX satellite surveyed the entire sky in two ultraviolet bands, 1344–1786 Å (FUV) and 1771–2831 Å (NUV), reaching an all-sky depth of $m_{AB} \sim 20$. More details of the mission can be found in Morrissey et al. (2005) and Martin & GALEX Team (2005).

#### 2.2.3. Optical photometry

The Blanco Cosmology Survey (BCS) observed $\sim 50$ deg$^2$ centred at $\alpha = 23^{h}00^{m}00^{s}$ and $\delta = -55^{\circ}00'00''$, giving full coverage of XXL-S. The Mosaic2 imager was used on the Cerro Tololo Inter-American Observatory (CTIO) 4-m Blanco telescope to generate data in the $griz$ bands, reaching 10 arcmin point-source depths of 23.9, 24.0, 23.6, and 22.1 mag (AB). More details can be found in Desai et al. (2012). In addition, the Dark Energy Camera (DECam; Flaugher et al. 2015) was used with the Blanco telescope to observe XXL-S (PI: C. Lidman) in the $griz$ bands (4850–9000 Å). The limiting magnitudes reached in each band (defined as the third quartile of the corresponding magnitude distribution) are 25.73, 25.78, 25.6, and 24.87 mag (AB). More details of the observations can be found in XXL Paper VI and a description of the data reduction can be found in Desai et al. (2012, 2015).

#### 2.2.4. Optical spectra

Spectra in the wavelength range of $\sim 370$–900 nm were gathered for thousands of objects in XXL-S in two observing runs in 2013 and 2016 with the Australian Astronomical Telescope (AAT) using the two-degree field (2dF) fibre positioner (Lewis et al. 2002) with the AAOmega spectrograph (Smith et al. 2004). The first run obtained 3660 reliable redshifts for X-ray selected objects (Lidman et al. 2016, XXL Paper XIV), 136 of which are also radio sources; the second run (PI: M. Plionis) obtained a total of 2813 reliable redshifts for a mix of X-ray, optical, and radio-selected objects (Chiappetti et al. 2017, XXL Paper XXVII, submitted). In the second run, 1148 radio sources whose optical counterparts are brighter than $r_{AB} < 22.0$ (equivalent to $r_{\text{Vega}} < 21.8$) were targeted, from which 986 reliable redshifts were obtained. Adami et al. 2011, Table 3 in XXL Paper I, Adami et al. (2017) (XXL Paper XX, submitted), and Guglielmo et al. (2017) (XXL Paper XXII) contain information on a few other spectroscopic surveys that covered XXL-S, but these surveys added a total of only 12 redshifts to the final sample of this paper.

#### 2.2.5. Near-infrared data

The Vista Hemisphere Survey (VHS) is observing the entire southern sky in the near-infrared (NIR) using the Visible and Infrared Survey Telescope for Astronomy (VISTA), and it has also observed the $\sim 5000$ deg$^2$ southern Galactic cap, which includes the whole of XXL-S. In this region, it reached 5$\sigma$ point-source depths of $J = 20.6$, $H = 19.8$ and $K_s = 18.1$ mag (Vega). More information can be found in McMahon et al. (2013).

#### 2.2.6. Mid-infrared data

The Wide-field Infrared Survey Explorer (WISE) mission observed the whole sky in four mid-IR bands: $W_1 = 3.4$ $\mu$m, $W_2 = 4.6$ $\mu$m, $W_3 = 12$ $\mu$m, and $W_4 = 22$ $\mu$m (Wright et al. 2010). The survey reached 5$\sigma$ depths of 16.5, 15.5, 11.2, and 7.9 mag (Vega), respectively. The WISE MIR data used in this paper was extracted with a fixed aperture 3$''$ wide at 1$\sigma$ depths of 17.62, 17.01, 13.50, and 10.64 mag (Vega), respectively. These have been matched to $\sim 15$ other filters in the multiwavelength catalogue for XXL-S (XXL Paper VI; Fotopoulou et al., in prep.), and are therefore unlikely to be spurious. Furthermore, the Spitzer satellite has observed the 94 deg$^2$ Spitzer South Pole Telescope Deep Field (SSDF), centred at $\alpha = 23^{h}00^{m}00^{s}$ and $\delta = -55^{\circ}00'00''$, with its Infrared Array Camera (IRAC; Fazio et al. 2004). This field fully covers XXL-S. IRAC channels 1 (3.6 $\mu$m) and 2 (4.5 $\mu$m) were used, reaching 5$\sigma$ (Vega) sensitivities of 19.0 and 18.2 mag (7.0 and 9.4 $\mu$Jy), respectively. Additional details can be found in Ashby et al. (2013).

### 2.3. Cross-matching procedure

This section summarises the method used to cross-match the radio sources to the multiwavelength catalogue.

#### 2.3.1. Initial radial match

The XXL-S radio source catalogue from XXL Paper XVIII was initially cross-matched to the sources in the multiwavelength catalogue from XXL Paper VI and Fotopoulou et al. (in prep.) using a simple radial match with a radius of 3$''$; the position for each source in the multiwavelength catalogue is based on the position in the highest resolution band available for the source. This produced a total of 6277 potential optical counterparts to all 6287 radio sources in XXL-S.

Figure 1 shows the histogram of the total number matches as a function of separation radius between the radio sources and all potential optical counterparts. The
non-zero offsets between the radio and optical positions are assumed to be due to measurement error alone, so the a priori infinitesimal probability \( dP_{\text{gen}} \) of a genuine optical match being found at a distance between \( r \) and \( dr \) for all the radio sources is given by the Rayleigh distribution (de Ruiter et al. 1977; Wolstencroft et al. 1986)

\[
dP_{\text{gen}} = \frac{N_{\text{gen}}}{\sigma^2_{\text{pos}}} r e^{-r^2/2\sigma^2_{\text{pos}}} dr, \tag{1}
\]

where \( N_{\text{gen}} \) is the number of radio sources with a highly probable genuine match (as determined by the likelihood ratio method described in Section 2.3.2) and \( \sigma^2_{\text{pos}} = \sigma^2_{r} + \sigma^2_{o} \) (\( \sigma_r \) is the radio positional uncertainty and \( \sigma_o \) is the optical positional uncertainty). In this work, \( N_{\text{gen}} = 4770 \), \( \sigma_r = 0.37'' \) (using the average radio positional uncertainty and assuming a simple model in which the RA and Dec radio positional uncertainties are symmetric), and \( \sigma_o = 0.30'' \). Entering these values into Equation 1 generated the genuine match curve shown in Figure 1. On the other hand, the probability \( dP_{\text{spur}} \) that a spurious optical match will be found between \( r \) and \( dr \) is given by

\[
dP_{\text{spur}} = N_{\rho}(2\pi r) dr, \tag{2}
\]

where \( N_{\rho} = 6287 \) is the total number of radio sources in XXL-S and \( \rho_0 \approx 127793 \) deg\(^{-2}\) is the globally averaged density on the sky of all \( z\)-band\(^1\) sources in XXL-S. Using these values for Equation 2 produced the spurious match line in Figure 1, which shows that the percentage of spurious matches rapidly increases beyond \( \sim 1'' \). For example, at \( \sim 1.3'' \), there are \( \sim 50\% \) spurious matches. While there are some genuine matches at large radii, using a simple radial match increases the contamination from spurious matches. In order to be able to capture as many genuine matches as possible while avoiding spurious matches, a more sophisticated technique is required.

### 2.3.2. Likelihood ratio

The likelihood ratio (LR) technique (Richter 1975; de Ruiter et al. 1977; Sutherland & Saunders 1992; Ciliegi et al. 2003) is useful for distinguishing between the probable genuine optical match to a radio source and unrelated background objects. The LR is defined as the ratio of the probability of a given optical source being the genuine counterpart of the radio source to the probability of the optical source being an unrelated background object. For a given potential optical counterpart with magnitude \( m \) and positional offset \( r \) from the radio source position, the LR is expressed as

\[
LR = \frac{q(m)f(r)}{n(m)}, \tag{3}
\]

where \( q(m) \) is the expected probability distribution of the true optical counterparts as a function of magnitude, \( f(r) \) is the probability distribution function of the combined radio and optical positional uncertainties (i.e. an elliptical Gaussian distribution representing the quadrature sum of the radio and optical positional uncertainties in RA and Dec)

\(^1\) The \( z\)-band was used because the data are deeper and galaxies are normally brighter in the infrared than they are at bluer wavelengths, so it gives access to a greater number of sources.
then only the optical source with the highest reliability was chosen as the counterpart in that band. The reliability is the relative likelihood that a potential optical counterpart is the genuine counterpart, given the other potential counterparts and the probability that the genuine counterpart was not detected \((1 - Q)\). It is defined as

\[
R_j = \frac{LR_j}{\sum_i (LR_i) + (1 - Q)},
\]

where \(LR_j\) is the LR value for the optical source being considered and \(\sum_i LR_i\) is the sum of the LR values for all potential counterparts (Ciliegi et al. 2003);

5. The seven LR catalogues from each band (\(gri\text{c}JHK\)) were merged into one master catalogue;

6. For a given radio source, if two or more potential counterparts with \(LR > LR_{\text{th}}\) existed in different bands in the master catalogue,
   (a) If all potential counterparts existed in one common band, the counterpart with the highest reliability in that band was chosen;
   (b) If none of the potential counterparts existed in at least one common band, the counterpart with the highest reliability in any band was selected.

Taking these steps resulted in 4770 radio sources that were cross-matched to a reliable optical counterpart. This is 76% of all radio sources in the ATCA XXL-S sample, which is consistent with previous radio-optical association studies at the same optical magnitude depth as XXL-S (see Ciliegi et al., in prep.). The number of potential misidentifications can be estimated by summing the \(1 - R_j\) values for all sources in each band. Of the seven bands used, the \(J\)-band was responsible for the lowest number of misidentifications \((\sim 36)\) and the DECAM \(z\)-band was responsible for the highest \((\sim 91)\). The average number of misidentifications across all bands is \(\sim 55\) sources, which is \(\sim 1.2\%\) of the 4770 optically matched radio sources.

2.4. Final sample

The number of radio sources that were cross-matched to optical sources using the LR technique is 4770 (Ciliegi et al., in prep.). There are 12 sources with AAT spectra that were classified as stars, so these sources were removed from the catalogue. The final sample used for the purposes of source classification in this paper is the set of 4758 radio sources that were cross-matched with the LR technique to the non-stellar optical sources in the multiwavelength catalogue from XXL Paper VI and Fotopoulou et al. (in prep.), as described in Section 2.3.2. The rest of this paper refers to this sample, unless otherwise stated.

2.4.2. Photometric redshift accuracy

The number of optically matched XXL-S radio sources for which a reliable spectroscopic redshift is available is 1110. For the remaining 3648 sources, the extensive photometric coverage of XXL-S was utilised to compute their photometric redshifts as described in XXL Paper VI and Fotopoulou et al. (in prep.). To summarise, a random forest machine-learning classifier was trained to distinguish between passive, star-forming, starburst, AGN and QSO galaxies according to their broadband colours (\textit{GRIZYJHK}, plus IRAC channel 1) and their \(I\)-band half-light radius. Given this class assignment, the photometric redshift of each source was computed with a restricted set of templates corresponding to each galaxy class.

The accuracy of photometric redshifts is usually estimated with two measurements: the normalised median ab-
Fig. 3. Comparison of $z_{\text{phot}}$ and $z_{\text{spec}}$ for the 1110 radio sources with a spectroscopic redshift. The red line represents $z_{\text{phot}} = z_{\text{spec}}$. The data points for which $z_{\text{phot}} = 0.01$ are those whose photometric redshift was degenerate enough to cause a poor fit.

The solute deviation (NMAD), defined as

$$\sigma_{\text{NMAD}} = 1.48 \left( \frac{|z_{\text{phot}} - z_{\text{spec}}|}{1 + z_{\text{spec}}} \right)_{\text{median}},$$

(5)

and the fraction of catastrophic outliers $\eta$, defined as the fraction of sources with $|z_{\text{phot}} - z_{\text{spec}}| > 0.15(1 + z_{\text{spec}}).$

(6)

For all radio sources in XXL-S, $\sigma_{\text{NMAD}} = 0.062$ and $\eta = 17\%$, and sources with $z_{\text{spec}} > 1$ exhibit $\sigma_{\text{NMAD}} = 0.156$. For comparison, the ∼2900 normal galaxies (i.e. without X-ray detections) with reliable spectroscopic redshifts in XXL-S show $\sigma_{\text{NMAD}} = 0.056$ and $\eta = 15\%$. The combined emission from AGN and their host galaxies creates difficulties for photometric redshift estimations (e.g. Brodwin et al. 2006; Salvato et al. 2009; Assef et al. 2010). However, the XXL-S photometric redshift performance is close to the expectation given the use of broadband filters and the lack of deep $u$-band and near-infrared observations (Table 4 in Salvato et al. 2009). Figure 3 shows the comparison between the available spectroscopic redshifts and their corresponding photometric redshifts. Figure 4 shows the redshift distribution of all 4758 optically matched radio sources, using spectroscopic redshifts where available. The distribution peaks at $z \sim 0.45$, and features a tail extending to $2 < z < 4$.

### 2.4.3. Radio spectral indices and luminosities

Figure 5 shows the distribution of the ATCA 1–3 GHz in-band radio spectral indices ($\alpha_R$) for all optically matched XXL-S radio sources for which a spectral index calculation is available (2974 sources). The median value is $\alpha_R \approx -0.45$, which is flatter than the value used in XXL Paper XVIII for XXL-S radio sources matched to Sydney University Molonglo Sky Survey (SUMSS) 843 MHz sources (−0.75). Appendix A describes the reason for this flatter median $\alpha_R$ value, and how the spectral indices were calculated and assigned. For comparison with other studies, the rest-frame 1.4 GHz monochromatic luminosity densities (hereafter luminosities) of the sources were calculated. First, each 2.1 GHz flux density was converted into a 1.4 GHz flux density ($S_{1.4\text{GHz}}$) using the $\alpha_R$ value for each source. Then the 1.4 GHz luminosity of each source was computed with the equation

$$L_{1.4\text{GHz}} = 4\pi d_L^2 S_{1.4\text{GHz}}(1 + z)^{-(1 + \alpha_R)},$$

(7)

where $d_L$ is the luminosity distance in metres, $z$ is the best redshift (spectroscopic if available, otherwise photometric), and $\alpha_R$ is the ATCA 1–3 GHz in-band radio spectral index. Figure 6 shows $L_{1.4\text{GHz}}$ versus redshift for each radio source with an optical counterpart.
3. Radio source classification

This section describes the multiwavelength diagnostics used to identify AGN and SFGs in the final optically matched radio sample. The diagnostics are based on X-ray luminosities and hardness ratios (Section 3.1); spectral energy distribution (SED) fitting (Section 3.2); MIR colours (Section 3.3); optical spectra (Section 3.4); optical colours (Section 3.5); and radio luminosities, spectral indices, and morphologies (Section 3.6). The decision tree used to classify the sources is detailed in Section 3.7.

3.1. X-ray classification

X-ray emission from AGN arises from inverse Compton scattering of lower energy photons by hot electrons and potentially from thermal emission at soft X-ray energies \((E < 2 \text{ keV})\) from the inner accretion disk. In particular, multiple scatterings within the hot electron corona result in a non-thermal power-law X-ray spectra for energies in the range \(1 \text{ keV} \leq E \leq 300 \text{ keV}\). The power law has the form \(F(E) \propto E^{-\Gamma}\); \(\Gamma\) is the photon index, which has a typical value of \(\Gamma = 1.4 - 1.6\) for radio-loud AGN and \(\Gamma = 1.8 - 2.0\) for radio-quiet AGN (e.g., Reeves & Turner 2000; Piconcelli et al. 2005; Page et al. 2005). On the other hand, Bauer et al. (2004) observed that the X-ray emission from local SFGs can be characterised by luminosities below \(L_{0.5-8\text{keV}} = 3 \times 10^{42} \text{ erg s}^{-1}\), and Colbert et al. (2004) found that SFGs are typically characterised by relatively soft emission with hardness ratios\(^2\) of \(HR < -0.1\) (corresponding to effective photon indices of \(\Gamma < 1\)). Therefore, following Juneau et al. (2013), each X-ray source was classified as an X-ray AGN if it had either \(L_{2-10\text{keV}} > 10^{42} \text{ erg s}^{-1}\) or \(HR > -0.1\).

\(^2\) In this paper, \(HR = (S_{\text{hard}} - S_{\text{soft}})/(S_{\text{hard}} + S_{\text{soft}})\)

There are 414 optically matched XXL-S radio sources with an X-ray counterpart that had flux measurements in at least one \(XMM\) band. If a source had flux measurements in both the 0.5–2 keV and 2–10 keV bands, its X-ray spectral index, \(\alpha_X\), was calculated according to

\[
\alpha_X = \frac{\log(S_{2-10\text{keV}}/S_{0.5-2\text{keV}})}{\log(E_{2-10\text{keV}}/E_{0.5-2\text{keV}})}
\]

(Schmidt & Green 1986), where \(E_{0.5-2\text{keV}}\) and \(E_{2-10\text{keV}}\) are the average energies in the 0.5–2 keV and 2–10 keV bands, respectively. This was converted into the X-ray photon index, given by

\[
\Gamma = \alpha_X + 1
\]

The median value of \(\Gamma\) for sources with a detection in both bands is \(\Gamma_{\text{med}} = 1.56\). The X-ray luminosity \(L_{2-10\text{keV}}\) was then calculated for each source according to the equation from Xue et al. (2011),

\[
L_{2-10\text{keV}} = 4\pi d_L^2 S_{2-10\text{keV}}(1 + z)^{-2},
\]

where \(d_L\) is the luminosity distance in cm, \(S_{2-10\text{keV}}\) is the observed flux in erg s\(^{-1}\) cm\(^{-2}\) in the 2–10 keV band, and \(z\) is the best redshift (spectroscopic if available, otherwise photometric). The observed flux is used because the fluxes in this sample are not high enough to constrain the amount of X-ray absorption. However, applying an absorption correction would not change the number of sources classified as X-ray AGN by a significant amount, and therefore using the observed X-ray fluxes has a negligible effect on the classification results. For sources with a detection in only one band, \(\Gamma_{\text{med}}\) was assumed for the calculation of their luminosities and hardness ratios. According to Xue et al. (2011), luminosities calculated in this way agree with the values derived from direct spectral fitting to within \(< 30\%\) (higher values are possible for heavily obscured AGN). However, the number of X-ray sources classified as X-ray AGN according to the criteria mentioned above is so high (412 out of 414, or 99.5\%) that an increase in the accuracy of the X-ray luminosities would not have a significant effect on the final classification results. Figure 7 shows a plot of \(L_{2-10\text{keV}}\) versus redshift for the 414 X-ray detected radio sources.

3.2. SED classification

The photometry of each radio source from optical to millimetre wavelengths was fit to identify possible evidence of AGN activity on the basis of a panchromatic SED-fitting analysis. The SED-fitting code MAGPHYS\(^3\) (da Cunha et al. 2008) and the three-component SED-fitting code SED3FIT\(^4\) by Berta et al. (2013), which accounts for an additional AGN contribution, were used to do this.

The MAGPHYS code is designed to reproduce a variety of galaxy SEDs, and relies on the energy balance between the dust-absorbed stellar continuum and the reprocessed dust emission at infrared wavelengths. However, it does not account for a possible AGN emission component. The SED3FIT code combines the emission from stars, dust heated by star formation, and an AGN (continuum and torus) component from the library of Feltre et al. (2012) and Fritz et al. (2006), resulting in a simultaneous three-component fit. In

\(^3\) http://www.iap.fr/magphys/magphys/MAGPHYS.html

\(^4\) http://cosmos.astro.caltech.edu/page/other-tools
order to quantify the relative likelihood of a possible AGN component, the approach from Delvecchio et al. (2014) was followed: each source’s SED was fit with both the MAGPHYS and SED3FIT codes. The reduced \( \chi^2 \) values of the SED fits with and without the AGN were calculated. If the reduced \( \chi^2 \) of the fit with the AGN was significantly smaller than that of the fit without the AGN (at the \( \geq 99% \) confidence level on the basis of a Fisher test, as found in Bevington & Robinson 2003), then that source was considered to have a significant AGN component in its SED.

This approach resulted in the identification of 988 radio sources that are considered AGN on the basis of their SED fits. The remaining 3770 sources were classified as non-AGN according to their SED fit (see Section 3.2), the blue circles are sources classified as AGN according to their SED fit (see Section 3.2), the cyan circles are both MIR and SED AGN, and the black points are all other X-ray detected radio sources.

### 3.3. Mid-infrared classification

At MIR wavelengths of \( \lambda = 5–10 \, \mu m \), the MIR SEDs of SFGs are dominated by broadband emission from polycyclic aromatic hydrocarbons (PAHs), which exhibit emission features mainly at 3.3, 6.2, 7.7, 8.6, and 11.3 \( \mu m \). At longer wavelengths of \( \lambda \geq 20 \, \mu m \), the SEDs are dominated by thermal continuum emission from larger warm dust particles (Draine 2003). If an AGN is present, they can also contain higher temperature dust at \( T = 50 – 300 \, K \), whose radiation peaks at \( \lambda \sim 20 \, \mu m \). AGN can also destroy PAH molecules via their strong UV radiation, thus damping PAH emission. This results in a decrease in the relative contribution of PAH to MIR continuum emission for warmer galaxies, or lower PAH equivalent widths (Elbaz et al. 2011). Therefore, examining the MIR emission of galaxies at wavelengths corresponding to PAH emission features and the blackbody radiation of warm dust can assist in identifying AGN. The MIR AGN indicators used in this paper are explained in the next three subsections. A source was considered a MIR AGN if at least one of the MIR criteria was met.

#### 3.3.1. WISE colour-colour diagrams

In general, AGN exhibit redder MIR colours than normal galaxies. For example, the WISE AGN wedges in Mateos et al. (2012) are defined to include all objects with MIR colours expected for power-law SEDs with spectral index \( \alpha_{IR} \leq -0.3 \). Assuming that X-ray luminosity in the 2–10 keV band is a good tracer of AGN activity, Mateos et al. (2012) demonstrated that their WISE selection has one of the highest reliabilities of all the MIR AGN indicators in the literature, with minimal contamination from high-redshift SFGs. Therefore, the Mateos et al. (2012) wedges for W1 – W2 versus W2 – W3, and W1 – W2 versus W3 – W4 were chosen to select MIR AGN.

The W1 – W2 versus W2 – W3 wedge is defined by the intersection of the following regions (Mateos et al. 2012):

1. Top edge: W1 – W2 < 0.315(W2 – W3) + 0.796
2. Left edge: W1 – W2 > -3.172(W2 – W3) + 7.624
3. Bottom edge: W1 – W2 > 0.315(W2 – W3) – 0.222

Figure 9 shows the W1 – W2 versus W2 – W3 plot for the XXL-S radio sources with W1, W2, and W3 data available. Of the 393 sources with WISE bands 1–3 available, 71 were classified as MIR AGN.

The W1 – W2 versus W3 – W4 wedge is described by the intersection of the following regions (Mateos et al. 2012):

1. Top edge: W1 – W2 = 0.5(W3 – W4) + 0.979
2. Left edge: W1 – W2 = -2(W3 – W4) + 4.33
3. Bottom edge: W1 – W2 = 0.5(W3 – W4) – 0.405

Figure 10 shows the WISE W1 – W2 versus W3 – W4 diagram for the XXL-S radio sources with W1, W2, W3, and W4 data available. Of the 82 radio sources with WISE bands 1–4 available, 9 were considered MIR AGN.

---

**Figure 7.** X-ray luminosity in the 2–10 keV band (\( L_{2-10keV} \)) vs. redshift for XXL-S radio sources detected in at least one X-ray band. The red circles are galaxies classified as AGN according to their MIR colours (see Section 3.3), the blue circles are sources classified as AGN according to their SED fit (see Section 3.2), the cyan circles are both MIR and SED AGN, and the black points are all other X-ray detected radio sources.

**Figure 8.** Example of a source that required a significant AGN component in its SED fit. The blue line is the AGN component, the red line is the AGN component, and the black line is the total SED.
Fig. 9. WISE $W_1 - W_2$ vs. $W_2 - W_3$ diagram for XXL-S radio sources. The blue circles are galaxies that have been classified as AGN according to their SED fit, the red circles galaxies that have been classified as X-ray AGN, and the cyan circles both SED and X-ray AGN. The blue Mateos et al. (2012) wedge is the indicator used in this work. For comparison, the Jarrett et al. (2011) box (red) and the Stern et al. (2012) line (green) are shown.

Fig. 10. WISE $W_1 - W_2$ vs. $W_3 - W_4$ diagram for XXL-S radio sources. The blue circles are galaxies that have been classified as AGN according to their SED fit, the red circles galaxies that have been classified as X-ray AGN, and the cyan circles both SED and X-ray AGN. The solid curve is the 90% WISE reliability curve (Equation 11) and the dashed line is the 75% WISE completeness line ($W_1 - W_2 = 0.77$), both from Assef et al. (2013).

3.3.2. WISE colour-magnitude diagram

Only a small percentage (8%) of the XXL-S optically matched radio sources had at least WISE bands 1–3 available, yet 1375 had at least WISE bands 1 and 2. Therefore, a method was sought to include these sources in the analysis. Previous studies of MIR AGN selection relied on a simple colour cut in $W_1 - W_2$ (e.g. Stern et al. 2012). Those samples were brighter than the MIR sources in the XXL-S optically matched sample, so in order to maintain reliability for fainter sources, a magnitude-dependent $W_1 - W_2$ colour selection is needed. Assef et al. (2013) derived such a selection for WISE AGN in the NDWFS Boötes field, and thus the AGN selection criteria for $W_1$ and $W_2$ from that work are used in this paper.

Figure 11 shows the WISE colour-magnitude diagram ($W_1 - W_2$ versus $W_2$) for XXL-S radio sources with $W_1$ and $W_2$ data available. The 75% completeness line ($W_1 - W_2 = 0.77$, shown as the dashed line in Figure 11), and the 90% reliability curve (solid curve in Figure 11) were used to select MIR AGN. The latter is described by

$$W_1 - W_2 > \alpha \exp[\beta(W_2 - \gamma)^2].$$

where $\alpha = 0.662$, $\beta = 0.232$, and $\gamma = 13.97$ (Assef et al. 2013). The two lines intersect at $W_2 = 14.777$. This magnitude limit and the colour cut of $W_1 - W_2 = 0.77$ is very similar to the Stern et al. (2012) colour cut ($W_1 - W_2 \geq 0.8$ for $W_2 < 15.05$). Therefore, if the brighter MIR sources ($W_2 < 14.777$) had $W_1 - W_2 > 0.77$, they were classified as MIR AGN. If the fainter MIR sources ($W_2 > 14.777$) were above the curve described in Equation 11, they were also classified as MIR AGN. Of the 1375 sources with $W_1$ and $W_2$ data available, 129 were identified as MIR AGN.

Fig. 11. WISE $W_1 - W_2$ vs. $W_2$ for XXL-S radio sources. The blue circles are galaxies that have been classified as AGN according to their SED fit, the red circles galaxies that have been classified as X-ray AGN, and the cyan circles both SED and X-ray AGN. The solid curve is the 90% WISE reliability curve (Equation 11) and the dashed line is the 75% WISE completeness line ($W_1 - W_2 = 0.77$), both from Assef et al. (2013).

3.3.3. IRAC colour-magnitude diagram

IRAC colours using all four channels are commonly used to select AGN (e.g. Donley et al. 2012). However, only IRAC channels 1 and 2 (hereafter IRAC1 and IRAC2) are available for XXL-S. Nevertheless, the central wavelengths and spectral response functions for IRAC1 and IRAC2 are very similar to W1 and W2, respectively. Additionally, IRAC data is deeper than WISE, and therefore there are more...
sources with IRAC data available (4023 of the 4758 optically matched radio sources, as opposed to 1375 with \(W_1\) and \(W_2\)). Therefore, in order to make the most of the IRAC MIR data available for XXL-S, a colour-magnitude diagram similar to the one presented in the previous section was adopted for the IRAC1 and IRAC2 data. Figure 12 shows the IRAC colour-magnitude diagram (IRAC1 − IRAC2 versus IRAC2) for sources with IRAC data available in XXL-S.

In order to find the appropriate adaptation of the Assef et al. (2013) criteria to the IRAC data, the IRAC and WISE colours were compared. The median value for \(W_1 - \text{IRAC}_1\) is \(-0.2\), and for \(W_2 - \text{IRAC}_2\) it is \(-0.3\) (these offsets are roughly constant with magnitude). Therefore, the median difference between \(W_1 - W_2\) and IRAC1 − IRAC2 is 0.1. Inserting these values into Equation 11 resulted in

\[
\text{IRAC}_1 - \text{IRAC}_2 = \alpha \exp[\beta(\text{IRAC}_2 - 0.3 - \gamma)] - 0.1, \quad (12)
\]

where \(\alpha\), \(\beta\), and \(\gamma\) have the same values as for the WISE data.

Since \((\text{IRAC}_1 - \text{IRAC}_2) - (W_1 - W_2) = -0.1\), the 75% completeness line was modified to be \(\text{IRAC}_1 - \text{IRAC}_2 = 0.67\). This line and the curve described in Equation 12 intersect at \(\text{IRAC}_2 = 15.077\). Any source brighter than this was classified as a MIR AGN if it had \(\text{IRAC}_1 - \text{IRAC}_2 > 0.67\), and any source fainter than this was considered a MIR AGN if its \(\text{IRAC}_1 - \text{IRAC}_2\) value was above the curve in Equation 12. Of the 4023 optically matched XXL-S radio sources with IRAC data available, 251 were classified as MIR AGN.

3.3.4. Overlap between MIR AGN indicators

In summary, 278 optically matched radio sources were identified as AGN on the basis of their MIR properties (141 according to the WISE indicators and 251 according to the IRAC indicator). Figure 13 shows the overlap between the three WISE AGN indicators. It demonstrates that the W1 − W2 versus W2 MIR AGN indicator misses only 12 galaxies that are classified as MIR AGN by the other WISE indicators. In other words, the majority of sources only have W1 and W2 data available, but this is sufficient to capture most of the WISE AGN in the field. Figure 14 shows that there are 114 MIR sources that were identified as AGN according to any of the WISE and IRAC indicators. This means that 114 out of 141 (80.9%) of the WISE MIR AGN have \(\text{IRAC}_1 - \text{IRAC}_2\) colours such that they were also classified as AGN according to the IRAC-modified Assef et al. (2013) indicator. These Venn diagrams show that the IRAC and WISE AGN indicators are consistent with each other.
3.4. Optical spectra classification

The two AAT observing runs described in Section 2.2.4 added 6473 reliable spectroscopic redshifts to the data available for XXL-S, 1098 (23.3%) of which corresponded to non-stellar optical counterparts of XXL-S radio sources. Twelve additional sources had spectroscopic redshifts available from the other non-AAT surveys referred to in Section 2.2.4. In total, 1110 XXL-S radio sources have spectroscopic redshifts.

3.4.1. BPT diagram

The Baldwin-Phillips-Terlevich (BPT) diagram (Baldwin et al. 1981) was designed to distinguish between AGN and SFGs by utilising the ratios between emission lines generated by different ionisation mechanisms. They found that defining AGN and SFG regions in a log([OIII]/Hβ) versus log([NII]/Ha) plot was an excellent way to identify AGN. However, for XXL-S sources with z ≥ 0.36, the [NII] line (λ=658.527 nm) is outside the effective wavelength range of the AAOmega data (~375-893 nm), so only sources with z ≤ 0.36 were able to have the BPT diagnostic examined.

There are 522 sources with z < 0.36 for which spectra are available. The software ROBOSPECT (Waters & Holker 2013) was used to measure the equivalent widths (EW) of the [OIII], Hβ, [NII], and Hα lines in the spectra for each of these sources. A signal-to-noise ratio of S/N > 3 was required for each line to qualify a source for the BPT diagram. Of the 522 spectra with z < 0.36, 156 had [OIII], Hβ, [NII], and Hα emission line EWs with S/N > 3. The errors in log([OIII]/Hβ) and log([NII]/Ha) were computed according to:

\[
\sigma_{\text{log}[\text{OIII}]/H\beta} = \sqrt{\left(\frac{\sigma_{\text{EW}([\text{OIII}])}}{\text{EW}([\text{OIII}])}\right)^2 + \left(\frac{\sigma_{\text{EW}(H\beta)}}{\text{EW}(H\beta)}\right)^2} \ln(10) \quad (13)
\]

\[
\sigma_{\text{log}[\text{NII}]/H\alpha} = \sqrt{\left(\frac{\sigma_{\text{EW}([\text{NII}])}}{\text{EW}([\text{NII}])}\right)^2 + \left(\frac{\sigma_{\text{EW}(H\alpha)}}{\text{EW}(H\alpha)}\right)^2} \ln(10), \quad (14)
\]

where σ_{EW([OIII])}, etc., are the uncertainties in the equivalent widths of the corresponding lines.

Figure 15 shows the BPT diagram for the XXL-S radio sources at z < 0.36. The solid red line in the figure is the SFG–AGN dividing line from Kewley et al. (2001) and the black points are those for which EW([OIII]) > 5 Å, and the black points are those for which EW([OIII]) < 5 Å. The error bars were calculated according to Equations 13 and 14. The solid red line is the extreme starburst line from Kewley et al. (2001) and the dashed blue line is the star-forming galaxy line from Kauffmann et al. (2003).

3.4.2. [OIII] line luminosity

The [OIII] line (λ=500.824 nm) is a useful tool for identifying AGN as its EW traces the electron density of the narrow-line region surrounding the black hole and the ionising photon flux from the accretion disk (Baskin & Laor 2005). It has been used as a powerful indicator to distinguish between HERGs and LERGs in previous studies of these AGN populations. For example, Hardcastle et al. (2013) found that for their sample of ~2500 radio-loud AGN (S_{4GHz} > 0.5 mJy) with spectroscopic redshifts, classifying HERGs as having EW([OIII]) > 5 Å and LERGs as having EW([OIII]) < 5 Å resulted in very similar HERG and LERG samples to those obtained via manual visual classification of the same galaxies using the strength of lines such as [OIII], [NII], [MgII], [CIII], [CIV], or Lyα as HERG and LERG indicators. In addition, Ching et al. (2017) found that the EW([OIII]) = 5 Å dividing line between HERGs and LERGs is very consistent with their visual spectral classification scheme for the ~11000 radio sources in the LARGESS survey with reliable spectroscopic redshifts. Best & Heckman (2012) also employed this cut to distinguish between HERGs and LERGs.

Due to the effective wavelength range of AAOmega, only the sources with z ≤ 0.78 were able to have their [OIII] lines examined. There are 971 sources at z < 0.78 with spectra. Requiring the [OIII] line to have a S/N > 3 resulted in 428 sources. Of these, 268 have EW([OIII]) > 5 Å, and are therefore classified as HERGs. The remaining 160 sources have EW([OIII]) < 5 Å, so they could either be LERGs or SFGs depending on their optical spectral templates (Section 3.4.3), optical colours (Section 3.5), or radio properties (Section 3.6).
3.4.3. Optical spectral templates

For the 954 spectra that did not qualify for the BPT diagram, the full wavelength range of each of the spectra were examined in order to determine the source types responsible for the observed spectral characteristics. The spectra were required to have a continuum S/N > 3, resulting in 871 sources eligible for this analysis. The software MARZ [Hinton et al. 2016] was used to find the best fit spectral template for each of these sources. MARZ uses seven galaxy templates, but just two are used in this work to explicitly classify the radio sources: quasar and early-type absorption galaxy (ETAG). Figure 16 shows examples of spectra that correspond to these templates and two other MARZ templates. Quasars were classified as HERGs, and ETAGs were classified as LERGs if none of the other indicators showed HERG activity.

3.5. Optical rest-frame colours

For the radio sources with no spectra available or for which the spectra were not usable, optical colours were used for further classification if the X-ray, MIR, SED, or optical spectral analyses did not indicate HERG activity. Ilbert et al. (2010) used the rest-frame $M_{NUV} - M_g$ colours (not corrected for dust extinction) to separate the quiescent from the star-forming populations in a sample of 196000 galaxies classified by morphology and SED fits out to $z < 2$ in the $\sim 2$ deg$^2$ COSMOS field. The $M_{NUV} - M_g$ colour is a good indicator of the current versus past star formation activity (e.g. Martin et al. 2007; Arnouts et al. 2007), but the $M_{NUV} - M_r$ colours display a more easily identifiable separation between quiescent galaxies and SFGs. This is manifested in quiescent galaxies having, for a given $g - i$ colour, larger relative $NUV - u$ colour offsets compared to SFGs than they do for $NUV - r$ colours. In other words, for a given $g - i$ colour, there is a larger fractional offset between quiescent galaxies and SFGs for $NUV - u$ than there is for $NUV - r$.

The physical reason for this is that the $u$-band covers wavelengths slightly shorter than the 4000 Å break ($3000 \leq \lambda \leq 4000$ Å) as well as the [OII] line at 3727 Å, while the $NUV$ covers shorter wavelengths ($1800 \leq \lambda \leq 2800$ Å). This results in quiescent galaxies having larger values of $M_{NUV} - M_u$ because their ultraviolet luminosities drop off rapidly after the 4000 Å break. On the other hand, SFGs have smaller $M_{NUV} - M_u$ values because they do not display strong 4000 Å breaks and they possess a much larger population of young OB stars that emit large amounts of ultraviolet radiation in the $NUV$.

This is demonstrated in Figure 17, which shows the $M_{NUV} - M_u$ versus $M_g - M_r$ (hereafter $NUV - u$ versus $g - i$) plot for all radio sources in XXL-S with a spectrum available with continuum $S/N > 3$. The rest-frame colours were calculated from the MAGPHYS SED fits, and they have not been corrected for dust extinction. The sources classified as ETAGs according to MARZ tend to be found in the colour space defined by $NUV - u > 2.0$ and $g - i < 1.2$, and all other galaxies tend to be found outside that space. Of all ETAGs, 82.5% are found in that colour space. Of all galaxies that reside in that colour space, 76.9% are ETAGs. In addition, Figure 17 shows that there is a clear trend for the non-ETAG galaxies to exist on or below a linear relation between $NUV - u$ and $g - i$. Of all non-ETAG galaxies, 73.0% exist below the line defined by $NUV - u = 1.5(g - i) + 0.25$, shown as the black line in Figure 17. This indicates that most of the galaxies that have at least a moderate level of star formation in the sample have colours that fulfil $NUV - u < 1.5(g - i) + 0.25$. Galaxies that lie above this line have redder UV colours for a given $g - i$, suggesting that they exhibit less UV emission and therefore lower levels of star formation. Of the ETAGs, 91.2% of them exist above the line, and 59.6% of all galaxies with spectra above the line are ETAGs.

Therefore, sources are considered red (with levels of star formation consistent with quiescent galaxies) if they lie above the line defined by $NUV - u = 1.5(g - i) + 0.25$. All other galaxies are considered blue and star-forming. These colour cuts are similar to the $UVJ$ colours used by previous authors to separate quiescent and star-forming galaxies (Muzzin et al. 2013 and references therein). How the $NUV - u$ versus $g - i$ colours affected the final classification of each source depended on its radio properties.

3.6. Radio classification

A source was considered a radio AGN if at least one of the following radio criteria was met.

3.6.1. Luminosity

In normal galaxies, the radio continuum can be used to trace star formation via the relativistic electrons accelerated around magnetic fields in supernovae and the electrons interacting with ions in HII regions (Condon 1992). The 1.4 GHz radio luminosity of normal galaxies does not normally exceed $L_{1.4\text{GHz}} = 10^{24}$ W Hz$^{-1}$ (e.g. Sadler et al. 2002; Best et al. 2005). This luminosity corresponds to a star formation rate (SFR) of $SFR_{1.4\text{GHz}} \sim 600 M_\odot$ year$^{-1}$ assuming the 1.4 GHz SFR calibration of Murphy et al. (2011). Some extreme SFGs have higher SFRs than this. For example, Barger et al. (2014) found that high-$z$ submillimetre galaxies in the GOODS-N field have a characteristic maximum SFR of $\sim 2000 M_\odot$ year$^{-1}$. This SFR corresponds to a luminosity of $L_{1.4\text{GHz}} = 10^{24.5}$ W Hz$^{-1}$. Therefore, a radio source is considered a radio AGN if it has $L_{1.4\text{GHz}} > 10^{24.5}$ W Hz$^{-1}$. The number of sources that meet this criterion is 1789.

3.6.2. Spectral index

Radio continuum emission at frequencies below 30 GHz is dominated by non-thermal synchrotron emission from relativistic electrons, with thermal emission comprising only $\sim 10\%$ of the total emission at 1–3 GHz (Condon 1992; Peel et al. 2011). Both star formation and AGN activity produce synchrotron radiation, which exhibits a typical spectral index of $\alpha_R \sim -0.75$. Therefore, it is difficult to disentangle AGN from SFGs at frequencies around 1 GHz on the basis of radio spectral index alone. However, Thompson et al. (2006) demonstrated that the range of radio spectral indices expected in starburst galaxies for the 1–3 GHz range is $-1.0 < \alpha_R < -0.5$. Steep spectra ($\alpha_R > -1.0$) are generated by old electrons, whereas flat spectra ($\alpha_R > -0.5$) correspond to multiple components in the line of sight or a recent outburst of electrons (e.g. Kellermann 1966; Kellermann & Pauliny-Toth 1969), both of which only AGN can produce. Therefore, applying a similar criterion to that used
Fig. 16. Example spectra (green) with corresponding Marz best fit templates (red), absorption lines (green dashed lines), and emission lines (blue dashed lines). The spectra have been smoothed for clarity. The best fit spectral templates are (from top to bottom) quasar, late-type emission galaxy, high redshift star-forming galaxy, and early-type absorption galaxy (ETAG).

by Rawlings et al. (2015), if a radio source has a 1σ upper bound of \( \alpha_R < -1.0 \) or a 1σ lower bound of \( \alpha_R > -0.5 \), it is considered a radio AGN. The number of sources identified as radio AGN according to their radio spectral indices is 766.

3.6.3. Morphology

The radio morphology of each of the complex radio sources, including those with multiple components (see Sections 3.6–3.8 in XXL Paper XVIII) was inspected. Nearly all of these sources are resolved. If the structure of a source’s radio contours displayed double lobes, jets, extended emission away from the host galaxy, or elongation perpendicular to the major axis of the optical host galaxy, then the source was classified as a radio AGN (see the left panel of Figure 18 for examples). The number of sources that were considered AGN according to their radio morphology is 401. There are six nearby disk galaxies for which the origin of the radio morphology cannot be determined, as revealed by the fact that the overall orientation of the radio contours is consistent with that of the host galaxy and the contours do not extend well beyond the disk (see the right panel of Figure 18 for examples). Only if none of the other AGN indicators were positive were these galaxies classified as SFGs. Of the six galaxies without definite radio AGN morphology, three have final classifications as HERGs (one radio-loud and two radio-quiet), two are classified as SFGs, and one is an unclassified source.

3.6.4. Luminosity excess

The \( SFR_{1.4\,\text{GHz}} \) calibration of Murphy et al. (2011) implies that the radio luminosity of a galaxy is directly proportional to its SFR. Therefore, if a galaxy has a radio luminosity greater than is expected from star formation, it is reasonable to assume that the excess luminosity is due to the presence of a radio AGN. In order to determine what level of radio excess would be appropriate to select radio AGN, the ratio of \( L_{1.4\,\text{GHz}} \) to the SFR computed by the MAGPHYS SED fitting \( (SFR_{\text{MP}}) \) was plotted versus EW([O iii]), which is shown in Figure 19. The vertical dashed line represents \( \text{EW}([\text{O iii}]) = 5 \), so none of the sources to the left of this line are HERGs according to the classification scheme. The red
Fig. 17. NUV – u vs. g – i for all radio sources in XXL-S that possess a spectrum with continuum S/N > 3. The colours have not been corrected for dust extinction. The red squares represent the galaxies classified as early-type absorption galaxies (ETAGs) according to their spectra and the black points represent all the galaxies that were not classified as ETAGs according to their spectra. The ETAGs tend to be found in the colour space defined by NUV – u > 2.0 and g – i < 1.2.

In addition, the radio excess distribution of the sources that were not identified as radio AGN by the previous three radio indicators suggests that at least two source populations contribute to the distribution (see inset in Figure 19). It is assumed that the portion of the distribution responsible for the peak at log(L1.4GHz/SFRMP) = 21.75 represents the SFG population due to the relatively low radio excess values. A Gaussian function was fit to this part of the distribution, which is shown by the red curve in the inset in Figure 19. The standard deviation of this Gaussian function is 0.25 in log(L1.4GHz/SFRMP) space. Therefore, the radio excess level that is 3σ above the Gaussian peak is log(L1.4GHz/SFRMP) = 22.5, which is the solid vertical black line in the inset. Therefore, in order to select previously unidentified radio AGN in the most reliable way possible, all sources with a radio excess of L1.4GHz/SFRMP > 10^{22.5} (W Hz^{-1})/(M_{\odot} year^{-1}) were considered radio AGN. This indicator identified 3418 radio AGN, 1390 of which were not identified by the other three radio indicators.

Table 1. Results of classification of XXL-S radio sources. Unclassified AGN potentially include LERGs and RL HERGs, while unclassified sources potentially include LERGs, RL HERGs, and SFGs.

| Source type     | Number | Fraction of final sample |
|-----------------|--------|--------------------------|
| LERGs           | 1729   | 36.3%                    |
| RL HERGs        | 1159   | 24.4%                    |
| RQ HERGs        | 296    | 6.2%                     |
| SFGs            | 558    | 11.7%                    |
| Unclassified AGN| 910    | 19.1%                    |
| Unclassified sources | 106  | 2.2%                     |

3.7. Decision tree

Figure 21 shows the decision tree by which the optically matched radio sources were classified. If a source displayed evidence of AGN activity via the X-ray, MIR, SED, or optical spectra indicators, then it was considered a HERG. If one of the radio indicators determined that the source contained a radio AGN, it was classified as a radio-loud (RL) HERG. If a radio AGN was not detected, then this suggested that the origin of the radio emission in the galaxy was star formation (not AGN activity), and so these sources were classified as radio-quiet (RQ) HERGs (e.g. Padovani et al. 2011; Bonzini et al. 2013).

If HERG activity was not detected, the optical spectrum of the source, if available, was examined. If the source was in the AGN region of the BPT diagram, it was classified as a LERG. If it was in the SFG region of the BPT diagram, it was classified as a LERG if a radio AGN was detected, and it was classified as a SFG otherwise. If the source was between the Kauffmann et al. (2003) and Kewley et al. (2001) lines in the BPT diagram, its NUV – u versus g – i colours were checked. If it was at z > 0.36 (meaning the BPT diagnostic was unavailable), its best fit optical spectral template was examined. If its spectrum was determined to be that of an ETAG, then it was classified as a LERG. If not, then its NUV – u versus g – i colours were also checked.

If a source had colours that fulfilled NUV – u > 1.5(g – i) + 0.25, the galaxy was considered red. Of these galaxies, if a source met one of the radio AGN criteria, it was classified as a LERG. If it did not exhibit signs of a radio AGN, it was left as an unclassified source. A source was considered blue if its colours were NUV – u < 1.5(g – i)+0.25. If a blue galaxy showed no signs of a radio AGN, then it was classified as an SFG. Otherwise, it was left as an unclassified AGN.

The classification process resulted in 1729 LERGs (36.3%), 1159 RL HERGs (24.4%), 296 RQ HERGs (6.2%), and 558 SFGs (11.7%), with 910 unclassified AGN (19.1%) and 106 unclassified sources (2.2%). Unclassified AGN potentially include LERGs and RL HERGs, while unclassified sources potentially include LERGs, RL HERGs, and SFGs. These results are summarised in Table 1, with the redshift dependence shown in Figure 20.
4. Discussion

4.1. AGN selection effects

A number of different factors lead to AGN being detected in one wavelength regime but not another. If a galaxy is particularly dusty, the MIR signal from the galactic dust may overpower the MIR signal from the dusty torus near the AGN, causing the relative MIR contribution from the AGN to be low and resulting in MIR colours that are outside of the domain of the MIR AGN indicators. It is also possible for a normal galaxy to have an AGN with a relatively small amount of dust, leading to a weak MIR signal from the AGN. For example, Hickox et al. (2009), who describes host galaxy properties of AGN in the ~9 deg² NOAO Deep Wide-Field Survey (NDWFS) field (Jannuzi & Dey 1999), found that most of their X-ray AGN are not selected by the IRAC MIR colour-colour criteria in Stern et al. (2005). They concluded that the MIR emission in the IRAC bands from those host galaxies probably mask a relatively low-luminosity IR-faint AGN (Gorjian et al. 2008). In addition, the X-ray emission from an AGN may be obscured by the dusty torus, resulting in an AGN that is classified as a MIR AGN but not an X-ray AGN. Compton-thick (n_H ≥ 10^{24} cm^{-2}) AGN are difficult to detect even in hard X-rays. For example, Mendez et al. (2013) found that 10 – 25% of MIR selected AGN in the Prism Multi-object Survey (Coil et al. 2011) are not classified as X-ray AGN, depending on the depth of the X-ray data. Radio AGN are not affected by dust, so they are still detectable in dusty galaxies. Since not all AGN can be detected in the same way, it is important to examine the overlap (or lack thereof) between AGN selected by different techniques.

4.1.1. Comparison of AGN classification techniques

The reliability and completeness of each of the AGN selection techniques presented in this work are an important quantification of the uniqueness of the AGN populations detected by each indicator. That is, the reliability and completeness of each indicator probe the degree to which other indicators can detect the overall AGN signal in the same objects. In this analysis, the reliability and completeness for a given indicator are defined as follows. Reliability is the percentage of sources detected by the indicator that are detected by another given indicator. Completeness is the percentage of all XXL-S AGN that are detected by the given indicator. All XXL-S AGN include LERGs, HERGs, and unclassified radio AGN.

Table 2 summarises the reliability and completeness of each AGN indicator. The reliability and completeness for the [O_III] indicator is of limited use as only 428 (9.0%) of the 4758 XXL-S optically matched radio sources have a spectrum with the [O_III] emission line at S/N > 3 available. Therefore, the [O_III] completeness applies only to those 428 sources (but the [O_III] completeness relative to all XXL-S AGN is still displayed in Table 2 for consistency). In the table, the reliability of each indicator is read from left to right. For example, the percentage of radio AGN that are SED AGN is 24.2%. In other words, the reliability of radio AGN in terms of SED AGN is 24.2%. The completeness of each indicator is read from top to bottom. For example, MIR AGN probe 6.8% of all AGN in XXL-S. In other words, the completeness of MIR AGN in terms of all AGN in XXL-S is 6.8%.

Radio AGN are limited in their ability to probe other AGN populations at the ~30% level. In other words, ~70% of radio AGN can be found only in the radio. This is mostly due to the LERGs in the sample, which do not show signs of AGN other than at radio wavelengths. In addition, there is a large fraction of [O_III]-only AGN, which are bright and at relatively low redshift (z < 0.78). This demonstrates the importance of spectra for finding HERGs.
Table 2. Reliability and completeness of AGN selection techniques. For reliability, the table should be read from left to right. For example, the percentage of X-ray AGN that are MIR AGN is 25.7% and the percentage of radio AGN that are any other kind of AGN is 30.5%. For completeness, the table should be read top to bottom. For example, X-ray AGN probe 16.1% of SED AGN and MIR AGN probe 23.5% of [O\textsc{iii}] AGN.

|                | X-ray | MIR | SED | [O\textsc{iii}] | Radio | Any |
|----------------|-------|-----|-----|-----------------|-------|-----|
|                | 25.7% (106/412) | 21.1% (87/412) | 28.6% (159/412) | 2.9% (109/412) | 30.5% (1155/3791) |
| X-ray          | 38.1% (106/278) | 22.7% (63/278) | 67.6% (188/278) | 88.5% (246/278) |
| MIR            | 16.1% (159/988) | 5.4% (53/988) | 93.0% (919/988) | 97.3% (961/988) |
| [O\textsc{iii}]| 32.5% (87/268) | 19.8% (53/268) | 64.0% (178/268) | 66.0% (177/268) |
| Radio          | 8.1% (307/3791) | 24.2% (919/3791) | 2.9% (109/3791) | 30.5% (1155/3791) |
| All            | 10.1% (412/4087) | 6.8% (278/4087) | 24.2% (988/4087) | 6.6% (268/4087) | 92.8% (3791/4087) |

Fig. 19. $L_{1.4\text{GHz}}/\text{SFR}_{\text{MP}}$ vs. EW([O\textsc{iii}]) for all XXL-S radio sources that possess a spectrum with continuum S/N > 3. The vertical dashed line represents EW([O\textsc{iii}]) = 5 Å (the dividing line between HERGs and LERGs/SFGs) and the horizontal solid line represents $L_{1.4\text{GHz}}/\text{SFR}_{\text{MP}} = 10^{22.5}$ (W Hz$^{-1}$) (M$_\odot$ yr$^{-1}$). The red squares represent the galaxies classified as early-type absorption galaxies (ETAGs) according to their spectra and the black points represent all other sources with the [O\textsc{iii}] line available. The ETAGs tend to be found in the space defined by $L_{1.4\text{GHz}}/\text{SFR}_{\text{MP}} > 10^{22.5}$ (W Hz$^{-1}$) (M$_\odot$ yr$^{-1}$) and EW([O\textsc{iii}]) < 5 Å (the upper left quadrant), and the vast majority of non-ETAG sources are outside this space. This suggests that the galaxies in the upper left quadrant of the plot are likely to be LERGs. The inset shows the distribution of log($L_{1.4\text{GHz}}/\text{SFR}_{\text{MP}}$) for sources that have not been identified as radio AGN by the other three radio indicators. The red curve is the Gaussian fit to the portion of the distribution that is assumed to be representative of the SFG population, and the vertical black line represents log($L_{1.4\text{GHz}}/\text{SFR}_{\text{MP}}$) = 22.5. The latter value is 3σ above the SFG population’s Gaussian peak.

4.1.2. X-ray versus MIR versus radio selection of AGN

Figure 22 displays the overlap between X-ray AGN, MIR AGN, and radio AGN in XXL-S. The AGN for each wavelength regime are defined as having at least one positive in any of the corresponding indicators. The sample in this paper is radio selected, so there are many more radio AGN than other classes of AGN. A large portion (69.4%) of the radio AGN represented in the diagram are classified as AGN by the radio indicators only (i.e. LERGs). This illustrates the prominence of the LERG population. The remaining radio AGN are HERGs that were classified according to their SED fits, EW([O\textsc{iii}]), or quasar spectral template, which are not taken into account in the diagram.

Of all radio AGN, 10.8% ± 0.5% are also X-ray AGN or MIR AGN. This can be compared to the overlap found by Hickox et al. (2009). Even though their sample was optically selected (so there are X-ray and MIR AGN that are not radio detected) and even though they used a radio AGN threshold of $L_{1.4\text{GHz}} > 10^{23.8}$ W Hz$^{-1}$, they found a similar overlap: 11.7% ± 3.4% of the radio AGN in their sample are also X-ray AGN or MIR AGN.

Considering the other AGN in XXL-S, 25.7% of X-ray AGN are also MIR AGN, and 38.1% of MIR AGN are also X-ray AGN. Even though XXL-S is radio selected, the latter percentage is similar to that found for X-ray-selected samples. For example, Donley et al. (2012) constructed an IRAC-selected MIR AGN sample for the COSMOS field and found that 38% of the MIR AGN had X-ray counterparts, which rose to 52% with deeper X-ray data. This is nearly identical to what Mateos et al. (2012) found for the
Bright Ultrahard XMM-Newton survey (BUXS): 38.5% of the MIR AGN selected with the WISE bands 1–3 were detected in hard X-rays, which rose to 49.8% if deeper X-ray observations were used. Given the X-ray and MIR depths available for XXL-S, the overlap between X-ray and MIR AGN is consistent with that found for other surveys.

4.1.3. X-ray versus MIR versus SED selection of AGN

The SED fits of the sources give an extra dimension of information regarding the selection effects of different AGN identification techniques. Figure 23 displays the overlap between X-ray AGN, MIR AGN, and SED AGN. The MIR and SED AGN have the most overall overlap (67.6% of MIR AGN are also SED AGN), probably because the vast majority of the total energy of an AGN signal in the optical and IR bands occurs at MIR wavelengths. The SED AGN that are not MIR AGN show that the SED fitting process is more sensitive to the MIR bump (hot dust component). In other words, a significant AGN component in an SED fit may cause the MIR colours of a source to change but not fall within the AGN regions of one of the MIR indicators presented in this paper. On the other hand, the MIR AGN that are not SED AGN demonstrate that there is some contamination of normal galaxies in the AGN regions of the MIR indicators.

Furthermore, 38.6% of the X-ray AGN are also SED AGN. This is similar to what Marchesi et al. (2016) found in the Chandra COSMOS-Legacy Survey for an X-ray selected sample: ~32% of the COSMOS X-ray sources with photometric redshifts required an AGN component to their SED fits. This large fraction of X-ray only AGN is likely due to the fact that X-ray data are less affected by the host-galaxy contamination compared to optical and MIR data, or that there are some AGN with low amounts of dust. This is reflected in Figures 11 and 12, where at least some of the X-ray AGN are found in the normal galaxy regions.

4.1.4. X-ray/MIR/SED versus [OIII] versus radio selection of AGN

Figure 24 shows the overlap between sources classified as either X-ray/MIR/SED AGN, sources classified as radio AGN, and sources classified as [OIII] AGN (EW([OIII]) > 5 Å). About 66% of the [OIII] AGN are also classified as X-ray/MIR/SED/radio AGN. Although spectral coverage of the 4758 optically matched XXL-S radio sources is only ~23% complete, this clearly implies that at least some
Fig. 22. Venn diagram showing overlap between X-ray AGN, MIR AGN, and radio AGN for the optically matched radio sources in XXL-S.

Fig. 23. Venn diagram showing overlap between X-ray AGN, MIR AGN, and SED AGN for the optically matched radio sources in XXL-S. HERGs can only be identified by the signatures in their optical spectra. In fact, all 91 of the sources classified as AGN solely by their \([\text{O} \text{ iii}]\) emission lines are RQ HERGs. This is a further reflection of the observation that different selection techniques identify different populations of AGN.

4.1.5. Contamination of LERG and SFG populations

Notwithstanding differences in survey depths and selection techniques, the broad similarities between the overlap of different classes of AGN in XXL-S and that of other multi-wavelength samples of AGN suggests that the HERGs and LERGs in XXL-S have been robustly classified and the overall picture of the different classes of AGN representing distinct populations of sources is generally valid.

However, the spectral coverage of XXL-S is \(\sim77\%\) incomplete. If it were more complete, more HERGs would be detected out of the population of sources classified by colours. Accordingly, it is useful to estimate the number of potential HERG sources that exist in the populations classified as LERGs and SFGs. It is assumed that HERGs are missed due to an unavailable optical spectrum. Of the 445 HERGs (either RL or RQ) that are red (the colour that corresponds to 99.0% of the LERG population), 415 (93.3%) are identified as either X-ray, MIR, or SED AGN. Therefore, 30 (6.7%) of the red HERGs could only be identified by their spectra (\(\text{EW}([\text{O} \text{ iii}]) > 5\ \text{Å}\) or a quasar spectral template). This means that \(\sim6.7\%\) (~93 sources) of the 1377 LERGs without spectra (i.e. identified by colours only) or \(\sim5.4\%\) of the whole LERG population could potentially be HERGs. On the other hand, of the 261 HERGs (either RL or RQ) that are blue and not classifiable as radio AGN (corresponding to the properties of 99.6% of the SFG population), 176 (67.4%) are identified as either X-ray, MIR, or SED AGN. So 85 (32.6%) blue HERGs not identifiable as radio AGN could only be identified by their spectra. This implies that out of the SFG population without spectra (385 sources), \(\sim32.6\%\) (~125 sources) or \(\sim22.5\%\) of the whole SFG population could potentially be HERGs. This is a high fraction of potential contaminants, but in terms of the HERG population only \(\sim125\) sources (~8.6%) have been potentially missed. This is the best that can be done with the available data. Of the LERG and SFG populations combined, \(\sim9.5\%\) (~218 sources) are potential HERGs.

4.2. The faint radio population

Figure 25 shows a plot of the relative fraction of radio source types as a function of \(S_{1.4\text{GHz}}\) (similar to Figure 6 in Bonzini et al. 2013). The plot only considers radio sources above the median 5\(\sigma\) ATCA XXL-S limit of \(\sim0.2\) mJy. The Poissonian errors of each fraction \(\sigma_{\text{frac}}\) (along the y-axis) are given by

\[
\sigma_{\text{frac}} = \sqrt{\frac{N_{\text{pop}}}{N_{\text{tot}}}}.
\]
where \( N_{\text{pop}} \) is the number of sources in a given population in a given \( S_{1.4\, \text{GHz}} \) bin and \( N_{\text{tot}} \) is the total number of sources in that \( S_{1.4\, \text{GHz}} \) bin. The area of the sky covered by the XXL-S radio survey at a given flux density is flux density dependent (see Figure 4 in XXL Paper XVIII), so each source is weighted by the inverse of the fraction of area covered in the radio mosaic at its corresponding flux density.

The figure shows that LRGs are more numerous than all HERGs between 1 mJy < \( S_{1.4\, \text{GHz}} \) < 10 mJy, but for \( S_{1.4\, \text{GHz}} \) ≤ 1 mJy, the combined fractions of RL and RQ HERGs become roughly equal to the LERG fraction, each accounting for ∼30% of the total radio source population. The RL HERG fraction decreases from ∼45% at \( S_{1.4\, \text{GHz}} \approx 15 \) mJy to ∼20% at \( S_{1.4\, \text{GHz}} \approx 2.75 \) mJy, and stays at this level down to \( S_{1.4\, \text{GHz}} = 0.2 \) mJy. The RQ HERG fraction is virtually non-existent for \( S_{1.4\, \text{GHz}} > 3.5 \) mJy, but steadily increases to ∼10% down to \( S_{1.4\, \text{GHz}} = 0.2 \) mJy. The unclassified AGN (which are a mix of LERGs and RL HERGs) rise steadily between 2 mJy < \( S_{1.4\, \text{GHz}} \) < 20 mJy to ∼25%, then flatten to a constant level of ∼15% for \( S_{1.4\, \text{GHz}} \leq 1 \) mJy. The unclassified sources (which are a mix of LERGs, RQ HERGs, and SFGs) make up a very small fraction of the total source population, accounting for ∼5% down to \( S_{1.4\, \text{GHz}} = 0.2 \) mJy.

All AGN (which include RL and RQ HERGs, LERGs, and unclassified AGN) make up ∼100% of the radio population at \( S_{1.4\, \text{GHz}} > 3 \) mJy (virtually no SFGs exist in that flux density regime). At \( S_{1.4\, \text{GHz}} \approx 0.3 \) mJy (the faintest flux density bin), AGN make up ∼75% of the radio source population. SFGs start becoming an appreciable fraction (∼10%) of the radio source population at \( S_{1.4\, \text{GHz}} < 1 \) mJy, and they reach up to ∼20% of the total down to 0.2 mJy. At the same flux density, Bonzini et al. (2013) found that SFGs make up ∼40% of the radio source population and AGN ∼60%. This is a significant disagreement (/>3σ) for the SFGs. However, Bonzini et al. (2013) classified 100% of the radio sources in their sample. They did not use spectra and SED fitting (which pick out AGN in galaxies that otherwise appear normal), and if any source did not exhibit at least one of their AGN indicators, it was classified as an SFG. Therefore, their classification method overestimates the relative fraction of SFGs.

The XXL-S results can also be compared to that of the 3 GHz data (converted to 1.4 GHz) for the low to moderate radiative luminosity AGN (MLAGN; HERG equivalent) and the moderate to high radiative luminosity AGN (HLAGN; HERG equivalent) sources in the COSMOS field (see Figure 12 in Smolčić et al. 2017). The HLAGN fraction in COSMOS, like the XXL-S HERG fraction, stays roughly constant at a mean value of ∼20–30% for 0.2 mJy < \( S_{1.4\, \text{GHz}} < 1 \) mJy. On the other hand, the XXL-S LERG fraction is ∼40% at 1 mJy and decreases to ∼30% at ∼0.3 mJy, whereas the MLAGN fraction in COSMOS is ∼70% between 0.65 mJy < \( S_{1.4\, \text{GHz}} < 1 \) mJy and stays between 40–50% between 0.2 mJy < \( S_{1.4\, \text{GHz}} < 0.55 \) mJy. If, however, the unclassified AGN in XXL-S were mostly LERGs, the XXL-S LERG fraction would be 15–20% higher, making both LERG fractions more similar. The XXL-S SFG fraction is higher (∼10%) than the COSMOS SFG fraction at 1 mJy (∼0%), but at 0.3 mJy, both fractions are similar (∼20%).

Despite slight discrepancies, the faint (≤1 mJy) radio source population in XXL-S broadly agrees with that of Bonzini et al. (2013) and Smolčić et al. (2017) over the same flux density range, showing a decline in the relative fraction of AGN and a steady rise of the SFG fraction with decreasing 1.4 GHz flux density.

### 4.3. Host galaxy properties of LERGs, HERGs, and SFGs

Table 3 summarises the median properties of the LERGs, HERGs, and SFGs in the optically matched XXL-S radio source sample. The decision tree used to classify the sources (Figure 21) allows for an independent derivation of the HERG host galaxy properties since the method used to identify HERGs does not make use of any previously discovered properties of HERG host galaxies. However, the LERGs and SFGs without classifiable spectra were selected largely on the basis of the properties of previously constructed LERG and SFGs samples (e.g. Best & Heckman 2012). In other words, LERGs are assumed to be red radio AGN and SFGs are assumed to be blue and not to conform to the radio AGN criteria as defined in Section 3.6. Therefore, this caveat should be considered when evaluating the differences between the properties of XXL-S HERGs, LERGs, and SFGs.

Figure 26a shows the 1.4 GHz luminosity (\( L_{1.4\, \text{GHz}} \)) and 1.4 GHz SFR (\( SFR_{1.4\, \text{GHz}} \)) distributions for each type of radio source. The \( L_{1.4\, \text{GHz}} \) values were calculated according to Equation 7 in this paper and the \( SFR_{1.4\, \text{GHz}} \) values were calculated according to Equation 17 from Murphy et al. (2011), converted to units of W Hz\(^{-1}\).

\[
SFR_{1.4\, \text{GHz}} = \left( \frac{L_{1.4\, \text{GHz}}}{1.575 \times 10^{21} \, \text{W Hz}^{-1}} \right) M_\odot \, \text{yr}^{-1}. \tag{16}
\]

A straight conversion between \( L_{1.4\, \text{GHz}} \) and \( SFR_{1.4\, \text{GHz}} \) is not valid for RL AGN, but allows a comparison to the optically
Fig. 26. (a) Rest-frame 1.4 GHz radio luminosity ($L_{1.4\text{GHz}}$, bottom axis) and 1.4 GHz SFR ($\text{SFR}_{1.4\text{GHz}}$, top axis) distributions for the LERGs, HERGs, and SFGs in XXL-S. LERGs and RL HERGs are found at all radio luminosities, but RL HERGs tend to have higher luminosities. The SFGs and RQ HERGs are cut off at $L_{1.4\text{GHz}} < 10^{24.5}$ W Hz$^{-1}$ because of the radio luminosity requirement for radio AGN. The high $\text{SFR}_{1.4\text{GHz}}$ values for LERGs and RL HERGs ($\geq 10^{3.3}$ M$_{\odot}$ yr$^{-1}$) are due to AGN contamination in their radio emission. (b) MAGPHYS stellar mass ($M_*$) distribution for the LERGs, HERGs, and SFGs in XXL-S. The host galaxies of LERGs have median $M_* \approx 10^{11.06}$ M$_{\odot}$, whereas HERGs and SFGs tend to be hosted by galaxies of lower median stellar mass (median $M_* \approx 10^{10.6} - 10^{10.8}$ M$_{\odot}$). (c) MAGPHYS star formation rate ($\text{SFR}_{\text{MP}}$) distribution for the LERGs, HERGs, and SFGs in XXL-S. LERGs exhibit low median SFRs ($\sim 2$ M$_{\odot}$ yr$^{-1}$) compared to that of HERGs and SFGs ($\sim 12-17$ M$_{\odot}$ yr$^{-1}$). (d) NUV – $u$ colour distribution for the LERGs, HERGs, and SFGs in XXL-S. The colours were derived from the MAGPHYS SED fitting. LERGs have redder median colours (NUV – $u \approx 2.21$) than RL HERGs (NUV – $u \approx 0.99$), RQ HERGs (NUV – $u \approx 1.12$), and SFGs (NUV – $u \approx 1.25$).

derived MAGPHYS SFR (see Figure 26c) because the excess between the MAGPHYS SFR and the 1.4 GHz SFR indicates AGN contamination in the radio. The high $SFR_{1.4\text{GHz}}$ values for LERGs and RL HERGs ($\geq 10^{3.3}$ M$_{\odot}$ yr$^{-1}$) are due to the radio emission from the AGN, not star formation. The figure shows that LERGs and RL HERGs are found at all radio luminosities, but there are more RL HERGs at higher luminosities ($L_{1.4\text{GHz}} > 10^{26}$ W Hz$^{-1}$), which is also what Best & Heckman (2012) found. The SFGs and RQ HERGs show a sharp cutoff at $L_{1.4\text{GHz}} < 10^{24.5}$ W Hz$^{-1}$ because of the radio luminosity criterion for radio AGN. The median $L_{1.4\text{GHz}}$ value for LERGs ($\sim 10^{24.1}$ W Hz$^{-1}$) is about one order of magnitude larger than that of SFGs and RQ HERGs ($\sim 10^{23.1}$ W Hz$^{-1}$), but approximately a factor of four below that of RL HERGs ($\sim 10^{24.7}$ W Hz$^{-1}$).

The stellar mass ($M_*$) and SFR ($\text{SFR}_{\text{MP}}$) distributions, both of which were derived as a result of the SED fits that MAGPHYS performed, are shown for each population in Figures 26b and 26c, respectively. The best fit stellar masses were used, but for the SFRs, the median $\text{SFR}_{\text{MP}}$ values were...
used instead because the lack of far-infrared constraints can result in a simultaneous overestimation of the SFR and an accurate fit to the SED at optical and near-infrared wavelengths. Nevertheless, some sources with poor photometry have high SFR values (>1000 M⊙ yr⁻¹), but there are just 119 of these sources, ~98% of which were classified as LERGs, HERGs, or unclassified AGN. LERGs tend to occupy galaxies with high stellar masses (median M∗ ≈ 10¹¹.06 M⊙) and low SFRs (median SFRMP ≈ 2 M⊙ yr⁻¹). On the other hand, HERGs and SFGs tend to occupy galaxies of lower stellar masses (median M∗ = 10¹⁰.6 - 10¹⁰.8 M⊙) and higher SFRs (median SFRMP ≈ 12–17 M⊙ yr⁻¹). The similarity in SFR for HERGs and SFGs is a reflection of the fact that this is a radio-selected sample, and therefore does not probe the whole SFG population in XXL-S.

Figure 26d shows the NUV – u colour distribution for LERGs, HERGs, and SFGs. The colours were also derived from the MAGPHYS SED fitting. LERGs tend to have redder colours (median NUV – u ≈ 2.21) than RL HERGs (median NUV – u ≈ 0.99). RQ HERGs (median NUV – u ≈ 1.25). Figure 27 shows the NUV – u versus g – i colours for each population. Only a small percentage (9.9%) of all HERGs are inside of the quiescent galaxy area of the plot (defined by NUV – u > 2 and g – i < 1.2), while 59.9% of the LERGs exist there. Most (69.4%) of the HERGs are blue, but the fraction of RQ HERG hosts that are blue (88.2%) is higher than the blue fraction of RL HERG hosts (64.6%).

LERGs and HERGs have a wide range of properties. For example, there are some LERGs that form stars just as rapidly as some HERGs (~100 M⊙ yr⁻¹), and there are some HERGs that are very red (NUV – u > 3). However, the overall properties of the LERG population are consistent with the idea that LERGs tend to exhibit lower radio luminosities and occupy the most massive, reddest, quiescent galaxies. In addition, the properties of the RL HERG population are consistent with sources that are more radio luminous and hosted by less massive, bluer galaxies that tend to form stars at frequencies as normal SFGs. The host galaxies of RQ HERGs are also characterised by bluer colours, lower masses, and ongoing star formation. These results are similar to what numerous other authors have found (e.g. Kauffmann et al. 2003; Best et al. 2005; Janssen et al. 2012; Best & Heckman 2012; Hardcastle et al. 2013; Best et al. 2014; Pracy et al. 2016; Ching et al. 2017).

5. Summary and conclusions

This work presented the results of the optical counterpart matching, classification, and characterisation of the 2.1 GHz radio sources in the 25 deg² XXL-S field, which is thus far the largest area radio survey conducted down to rms flux densities of ~41 µJy beam⁻¹. The likelihood ratio (LR) technique was applied to the XXL-S multiwavelength catalogue in order to find the most likely optical hosts of the radio sources. The technique found reliable counterparts for 4770 radio sources, 4758 of which were included in the final sample. These optically matched radio sources were then classified according to X-ray, MIR, SED, and radio diagnostics, as well as optical spectral templates, emission lines and colours. A decision tree was employed to determine a final classification for each source based on the results of each diagnostic.

The overlap between X-ray, MIR, and radio AGN in XXL-S is very similar to that of other multiwavelength studies of radio galaxies and AGN (e.g. Hickox et al. 2009), which, despite slight differences in the classification methods, validates the idea that different classes of AGN represent distinct populations of sources. Given the depth of the radio survey and the multiwavelength catalogue, and the completeness of the spectral coverage, the contamination of the combined LERG and SFG population by HERGs is estimated to be relatively low (~10%). The fractions of sub-mJy (S₁.4GHz < 1 mJy) sources that are AGN and SFGs are similar to the fractions found by Bonzini et al. (2013) and Smolčić et al. (2017) over the same flux density range, with ~75% definite radio AGN and ~20% SFGs down to 0.2 mJy.

The median properties of the HERGs in XXL-S were found to agree with what other similar studies have found, while the selection of the LERGs and SFGs without spectra was based on the properties of previously constructed samples of those populations (e.g. Best et al. 2005; Janssen et al. 2012; Best & Heckman 2012; Hardcastle et al. 2013; Best et al. 2014; Pracy et al. 2016; Ching et al. 2017).

Table 3. Median properties of LERGs, HERGs, and SFGs in XXL-S. The estimation of log[SFR₁.4GHz] does not apply to LERGs and RL HERGs because their radio emission is contaminated by AGN activity.

| Property                                      | LERGs | RL HERGs | RQ HERGs | SFGs |
|-----------------------------------------------|-------|----------|----------|------|
| log[L₁.4GHz (W Hz⁻¹)]                        | 24.11 | 24.72    | 23.06    | 23.07|
| log[M∗ (M⊙)]                                 | 11.06 | 10.78    | 10.62    | 10.70|
| log(SFRMP (M⊙ yr⁻¹))                         | 0.33  | 1.08     | 1.22     | 1.14 |
| log(SFR₁.4GHz (M⊙ yr⁻¹))                     | 1.87  | 1.87     | 1.87     | 1.87 |
| NUV – u                                       | 2.21  | 0.99     | 1.12     | 1.25 |

Fig. 27. NUV – u vs. g – i for LERGs (open red squares), RL HERGs (blue dots), RQ HERGs (filled purple circles), and SFGs (green crosses) in XXL-S. Many (~70%) of the HERGs exist in the same colour space as the SFGs. Only a small percentage (9.7%) of the HERGs are inside of the quiescent galaxy area of the plot (defined by NUV – u > 2 and g – i < 1.2), whereas 59.9% of LERGs exist inside that area.
whereas the HERGs and SFGs exist in galaxies of lower mass ($M_* \approx 10^{10.7} M_{\odot}$), higher SFRs ($\sim 15 M_{\odot} \cdot yr^{-1}$) and bluer colours (NUV $- u \approx 1.25$). The host galaxies of RQ HERGs have similar properties to RL HERGs, but RQ HERGs have a higher fraction of blue hosts. LERGs and RL HERGs are found at all radio luminosities, but RL HERGs tend to be more radio luminous (median $L_{1.4GHz} \sim 10^{24.7}$ W Hz$^{-1}$) than LERGs (median $L_{1.4GHz} \sim 10^{24.1}$ W Hz$^{-1}$). This is consistent with the idea that HERGs tend to exist in the most massive quiescent galaxies with low star formation rates, indicating that they are fuelled by the hot (X-ray emitting) phase of the IGM typically found in clusters, which limits their radiative output to radio wavelengths. It is also consistent with the idea that HERGs are associated with galaxies that have undergone recent star formation, indicating that their accretion material is cold gas from the IGM.

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where \( \sigma \) for 1417 MHz was made, all the \( S \) value at high

| Central frequency (MHz) | Robust parameter | Image radius (arcmin) |
|-------------------------|------------------|----------------------|
| 1417                    | -2.0             | 31.4                 |
| 2100                    | 0.0              | 22.7                 |
| 2783                    | 0.3              | 16.7                 |

### Appendix A: radio spectral index calculations

XXL-S radio sources that are unresolved in the full 2 GHz ATCA bandwidth (the ‘full-band’) were considered for radio spectral index analysis. In order to calculate the in-band radio spectral indices of these sources, radio mosaics of XXL-S for three ATCA sub-bands at central frequencies of 1417 MHz, 2100 MHz, and 2783 MHz, all with bandwidths of 683 MHz, were constructed. The steps taken to image every pointing in each of these three sub-bands were identical to those for the full-band (see Sections 2.3 and 2.4 in XXL Paper XVIII), with the following exceptions: robust parameters, image dimensions corresponding to the radii at which the primary beam responses are \(~8\%\) for the given central frequencies, a \( \text{SELFCAL} \) interval of 0.33 minutes (which was found to minimise the image artefacts around bright sources), and a \( \text{CONVOL} \) beam size of 6.36″ × 5.16″ with a position angle of 2.5°. Different robust parameters (corresponding to different visibility weighting distributions) were necessary in order to make the synthesised beam sizes for each sub-band as similar as possible before convolving the images. Table A.1 lists the central frequencies, robust parameters, and the radii the individual pointings were imaged out to for each sub-band. Once each pointing was imaged in each sub-band, the \( \text{MIRAD} \) (Sault et al. 1995) task \( \text{LINMOS} \) was used to combine and mosaic all the images together for each sub-band.

As for the full-band, \( \text{BLOBCAT} \) was used to detect all sources in each sub-band. A detection threshold of 3.05 \( \sigma \), where \( \sigma \) is the local rms value, was used. The plot of the ratio of integrated flux density to peak flux density (\( S_{\text{int}}/S_p \)) versus signal-to-noise ratio (\( S/N \)) for 2100 MHz and 2783 MHz showed no abnormalities, but the plot for 1417 MHz showed a very slight systematic downward curve (see Figure A.1), similar to the curve described in Appendix A of XXL Paper XVIII, but less severe. A simple method used to correct the 1417 MHz \( S_{\text{int}} \) values was executed. An interpolation function was computed for the median \( S_{\text{int}}/S_p \) values in log-spaced \( S/N \) bins. Each \( S_{\text{int}} \) was corrected according to this function to change the value of \( S_{\text{int}} \) such that at all \( S/N \), the value of \( S_{\text{int}}/S_p \) was approximately equal to its value at high \( S/N \) (~1.02 in this case). After this correction for 1417 MHz was made, all the \( S_p \) values in each sub-band were corrected for bandwidth smearing in the same way as described in Section 3.5 of XXL Paper XVIII.

Next, the three sub-band source catalogues from \( \text{BLOBCAT} \) were individually cross-matched to the 6287 full-band radio sources in the XXL-S source catalogue (XXL Paper XVIII). Only radio sources that are unresolved in the full-band were considered for an in-band radio spectral index calculation, resulting in 4661 eligible radio sources. The full-band sources were not cross-matched to 843 MHz sources from the Sydney University Molonglo Sky Survey (SUMSS) catalogue because only 28 ATCA XXL-S sources were classified as radio AGN on the basis of radio spectral index alone, and none of them has a SUMSS counterpart within 52.8″ (the major axis of the SUMSS beam at the declination of XXL-S).

At this point, each eligible full-band radio source had either detections in all three sub-bands, detections in two sub-bands, or fewer than two detections. The spectral indices were calculated for the 3827 radio sources with at least two sub-band detections. If exactly two detections were available, the spectral indices were calculated in the normal way using

\[
\alpha_R = \frac{\log(S_{\text{high}}/S_{\text{low}})}{\log(\nu_{\text{high}}/\nu_{\text{low}})}
\]

where \( S_{\text{high}} \) is the peak flux density measured at the higher frequency \( \nu_{\text{high}} \) and \( S_{\text{low}} \) is the peak flux density measured at the lower frequency \( \nu_{\text{low}} \). If there were three detections, a linear regression was fit to the \( \log(S) \) versus \( \log(\nu) \) data. Since spectral indices are calculated in log space, the uncertainties on the spectral indices were calculated according to the formula (adapted from Ciliegi et al. 2003)

\[
\sigma_{\alpha_R} = \frac{\sqrt{\sum (\sigma_{S_p}/S_p)^2}}{\ln(\nu_{\text{high}}) - \ln(\nu_{\text{low}})}
\]

where the sum is over all sub-band peak flux densities \( S_p \) available for the source, \( \sigma_{S_p} \) is the uncertainty in the corresponding \( S_p \), and \( \nu_{\text{high}} \) and \( \nu_{\text{low}} \) are respectively the highest and lowest frequencies involved in the calculation.

Figure A.2 shows the plot of \( \alpha_R \) versus full-band peak flux density (\( S_{FB} \)) for the 3827 XXL-S radio sources with at least two sub-band detections. The median \( \alpha_R \) values for each \( S_{FB} \) bin are displayed in Table A.2. The survival analysis performed in XXL Paper XVIII for all XXL-S radio sources with \( S_{FB} \) < 5 mJy indicated a median

![Fig. A.1. \( S_{\text{int}}/S_p \) vs. \( S/N \) for the 1417 MHz sub-band detections. The red curves show the envelope by which the full-band sources were determined to be resolved or unresolved (Equations 3 and 4 in XXL Paper XVIII). The red circles represent the median \( S_{\text{int}}/S_p \) values and the error bars represent the standard deviation in \( S_{\text{int}}/S_p \) for each \( S/N \) bin.](image-url)
The median $\alpha$ whereas at the brightest bin (each $\alpha$ circles with connecting red line show the median spectral index calculations are available (black points). The red peak flux density ($S_p$) show a trend toward flatter spectral indices for sources with typical spectral indices and a relatively high ($S/N_{FB} = 11.3$ mJy) the median $\alpha$ is $-0.76$. This clearly shows a trend toward flatter spectral indices for sources with $S_{p,FB} \leq 0.5$ mJy.

$\alpha_R = -0.66^{+0.18}_{-0.07}$, which is consistent with all but the lowest $S_{p,FB}$ bin given in Table A.2. The data in the table clearly show a trend toward flatter spectral indices for sources with $S_{p,FB} \leq 0.5$ mJy, which roughly corresponds to a full-band signal-to-noise ratio of $(S/N)_{FB} \approx 10$. The flattening at low $(S/N)_{FB}$ is not inherent to the radio source population in XXL-S, but due to a selection effect caused by the different rms noise distributions in each sub-band mosaic, which are shown in Figure A.3. Table A.3 shows the peak rms values for each sub-band, indicating that the 2783 MHz sub-band has the highest peak rms value. Consequently, at low $(S/N)_{FB}$, if a source has a 2783 MHz detection the 3.05$\sigma$ detection threshold selects sources with flatter spectral indices. In other words, for a given 1417 MHz or 2100 MHz rms value, only sources with spectral indices flat enough to allow their 2783 MHz $S_p$ values to be above the 2783 MHz 3.05$\sigma$ detection threshold will be detected at 2783 MHz. Low $(S/N)_{FB}$ sources without a 2783 MHz detection may have typical spectral indices ($-1 < \alpha < -0.5$), but they are missed at 2783 MHz because they fall below the 2783 MHz 3.05$\sigma$ detection threshold, leaving them with two sub-band detections and therefore less constrained spectral indices than those with higher $(S/N)_{FB}$. Therefore, the low $(S/N)_{FB}$ source sub-sample contains a relatively low fraction of sources with typical spectral indices and a relatively high fraction of flat-spectrum sources ($\alpha_R > -0.5$). As a result, the $\alpha_R$ distribution for sources at low $(S/N)_{FB}$ is systematically skewed toward flatter spectral indices. This does not imply that the spectral indices at low $(S/N)_{FB}$ are incorrect, but that they indicate an incomplete sampling of all possible spectral indices of faint sources in the XXL-S radio source catalogue.

Figure A.4 shows the distribution of ATCA in-band radio spectral indices for the 3827 XXL-S full-band radio sources with at least two sub-band detections, separated into those with $(S/N)_{FB} < 10$ and those with $(S/N)_{FB} > 10$. The median spectral index for sources with $(S/N)_{FB} < 10$ is $\alpha_R = -0.40$, and the median for those with $(S/N)_{FB} > 10$ is $\alpha_R = -0.55$. Due to the systematic flattening of spectral indices at low $(S/N)_{FB}$, if a source had $(S/N)_{FB} < 10$ or $S_{p,FB} < 0.527$ mJy and did not have an in-band spectral index measurement, its spectral index was assigned to be the median of all sources with $(S/N)_{FB} > 10$, ($\alpha_R = -0.55$). If a source had $(S/N)_{FB} > 10$ and $S_{p,FB} > 0.527$ mJy, and did not have a spectral index measurement available the value of the spectral index was determined by the median $\alpha_R$ value in its corresponding $S_{p,FB}$ bin shown in Figure A.2. For sources with $S_{p,FB} > 150$ mJy and no $\alpha_R$ value, a value of

### Table A.2. Median radio spectral indices ($\alpha_R$) for given full-band peak flux density ($S_{p,FB}$) bins.

| $S_{p,FB}$ bin (mJy) | $\alpha_R$ |
|---------------------|-----------|
| 0.150 < $S_{p,FB}$ < 0.281 | -0.363    |
| 0.281 < $S_{p,FB}$ < 0.527 | -0.455    |
| 0.527 < $S_{p,FB}$ < 0.987 | -0.530    |
| 0.987 < $S_{p,FB}$ < 1.849 | -0.548    |
| 1.849 < $S_{p,FB}$ < 3.465 | -0.549    |
| 3.465 < $S_{p,FB}$ < 6.493 | -0.541    |
| 6.493 < $S_{p,FB}$ < 12.167 | -0.541    |
| 12.167 < $S_{p,FB}$ < 22.799 | -0.507    |
| 22.799 < $S_{p,FB}$ < 42.721 | -0.559    |
| 42.721 < $S_{p,FB}$ < 80.050 | -0.622    |
| 80.050 < $S_{p,FB}$ < 150.000 | -0.756    |

### Table A.3. Peak rms noise values for each ATCA sub-band.

| Sub-band (MHz) | Peak rms noise (mJy beam$^{-1}$) |
|---------------|----------------------------------|
| 1417          | 0.066                            |
| 2100          | 0.057                            |
| 2783          | 0.076                            |

---

\[Fig. A.2.\] ATCA in-band radio spectral index ($\alpha_R$) vs. full-band peak flux density ($S_{p,FB}$) for all XXL-S radio sources for which spectral index calculations are available (black points). The red circles with connecting red line show the median $\alpha_R$ values for each $S_{p,FB}$ bin. The width of each $S_{p,FB}$ bin is $0.273$ in log space. The median $\alpha_R$ for the faintest bin at $S_{p,FB} \approx 0.22$ mJy is $-0.36$, whereas at the brightest bin ($S_{p,FB} \approx 115$ mJy) the median $\alpha_R$ is $-0.76$. This clearly shows a trend toward flatter spectral indices for sources with $S_{p,FB} \leq 0.5$ mJy.

\[Fig. A.3.\] Distributions of the rms noise in the 1417 MHz (red), 2100 MHz (green), and 2783 MHz (blue) ATCA sub-bands. Table A.2 shows the peak rms values for each sub-band. The higher peak rms value for 2783 MHz means that low $(S/N)_{FB}$ sources with a detection in that band tend to have systematically flatter spectral indices than sources without a 2783 MHz detection.
Butler et al.: The XXL Survey: XXXI. Classification and host galaxy properties of 2.1 GHz ATCA XXL-S radio sources

**Fig. A.4.** Distribution of ATCA in-band radio spectral indices for XXL-S radio sources with at least two 3.05σ radio sub-band detections, separated into $(S/N)_{FB} < 10$ (black histogram) and $(S/N)_{FB} > 10$ (red histogram) sub-samples. The median spectral index for $(S/N)_{FB} < 10$ is $\alpha_R = -0.40$, whereas the median for $(S/N)_{FB} > 10$ is $\alpha_R = -0.55$.

$\alpha_R = -0.75$ was assumed. All sources with a spectral index calculation available were assigned their corresponding $\alpha_R$ value. Of the 3827 sources with at least two sub-band detections, 2974 were cross-matched to optical counterparts.