Feedback-enhanced algorithm for aberration correction of holographic atom traps

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Abstract

We show that a phase-only spatial light modulator can be used to generate non-trivial light distributions suitable for trapping ultracold atoms, when the hologram calculation is included within a simple and robust feedback loop that corrects for imperfect device response and optical aberrations. This correction reduces the discrepancy between target and experimental light distribution to the level of a few percent (root mean square error). We prove the generality of this algorithm by applying it to a variety of target light distributions of relevance for cold atomic physics.

Keywords: ultracold atoms, optical trapping, aberration compensation, computer generated holography

A recent area of interest in the field of cold atomic physics is the development of non-trivial spatially- and temporally-varying optical trapping geometries, with interesting examples already demonstrated using techniques including acousto-optic deflection [1–4], amplitude-modulation [5, 6] and phase-modulation [6–15] of trapping light. Optical traps generally offer increased trap complexity at small length-scales, but at the disadvantage of increased likelihood of small-scale potential roughness [16]. Any local roughness in the intensity of the light pattern creates a varying energy landscape, which could cause heating or fragmentation of the atom cloud [17].

Fourier-engineered optical traps (those based on phase-only spatial modulation of the light to tailor the intensity in the Fourier plane of an optical system) have predominantly taken the form of arrays of discrete traps [8, 9] or Laguerre–Gauss beams [10]. Recently, a new calculation method for phase-only holograms of arbitrary complexity directly addressed the issue of roughness. This algorithm, the mixed-region amplitude freedom (MRAF) [16] variant of the Gerchberg–Saxton iterative Fourier transform algorithm [18], calculates smooth and accurate light patterns for use as optical atom traps. However, other than in special cases [12], the output of this algorithm does not give high-quality optical traps when applied to real devices and must be further adjusted [11, 13, 14]. In this paper, we present a simple, robust and generally-applicable algorithm to improve the accuracy of optical traps generated by phase-only spatial light modulators (SLMs).

The phase modulation required to produce the optical traps is initially calculated using the MRAF algorithm. For a given target intensity \( T_1 \) in the Fourier (i.e. output) plane, this algorithm iteratively optimizes a proposed phase-only hologram by emphasizing accuracy of the electric-field amplitude within a subset of the output plane (known as the signal region). The target amplitude \( T_1 \) contains the pattern of interest plus a surrounding area with zero amplitude. The amplitude is unconstrained in the remainder of the output plane (the noise region). The target amplitude \( \sqrt{T_1} \) contains the pattern of interest plus a surrounding area with zero amplitude. The amplitude is unconstrained in the remainder of the output plane (the noise region). The zero-amplitude region between the target pattern and the unconstrained amplitude ensures that atoms trapped in the signal region cannot tunnel into whatever intensity distribution is generated in the noise region. Calculations of trap quality are performed considering only non-zero pixels within the signal region (a subset known as the measure region, which contains the target). Upon stagnation of the MRAF routine, the algorithm...
returns an optimized phase pattern \( \phi_1 \) on the SLM plane and a predicted intensity \( P_1 \), which closely resembles \( T_1 \), on the output plane.

Our apparatus for the production of red-detuned optical traps where atoms will be trapped in intensity maxima has been previously introduced in [11, 12]. A 1064 nm laser beam illuminates the full active area of an SLM. Each of the 256 × 256 pixels can impart 256 phase levels between 0 and \( 2\pi \) on the light, which is then focussed by a \( f = 100 \) mm achromatic doublet. The focal plane of the lens constitutes the Fourier plane, which is imaged using a camera.

The phase \( \phi_1 \) is applied to the SLM and an image of the resultant Fourier–plane intensity \( M_1 \) recorded. This output typically significantly deviates from \( T_1 \) due to aberrations in the optical system and imperfect device response. To solve the problem of this deviation, we have designed a simple iterative feedback algorithm to steer the light pattern within the signal region towards the initial target \( T_1 \), as shown in figure 1. The error signal for this feedback loop is the discrepancy \( D_1 \), which is quantified within the measure region as \( D_1 = \tilde{T}_1 - M_1 \), where \( i \) denotes the iteration number and the tilde signifies normalization. We normalize by the mean value of all pixels in the output brighter than 50% of the maximum target value. We choose this normalization as it is resistant to both low-level background noise and particularly bright, single-pixel, noise. A corrected target pattern \( \tilde{T}_{i+1} = \tilde{T}_1 + D_i \) is then generated which compensates for the discrepancies. This new target serves as the input for another iteration of MRAF, and generates a new phase \( \phi_{i+1} \). The whole process is repeated until the output pattern reaches a stagnation point, defined to be after three subsequent iterations of feedback which improve the root mean square (RMS) error \( \epsilon_i \) by less than a set tolerance value \( \eta \), i.e. when \(|\epsilon_i - \epsilon_{i-1}| < \eta \) for three subsequent values of \( i \). For the examples below we have set \( \eta = 0.01 \). The algorithm is sufficiently robust that successful pattern production does not require pre-calculated wavefront corrections, such as those provided by the SLM manufacturer or acquired using a Shack–Hartmann wavefront sensor.

In practice we have found that increased accuracy can be achieved by introducing a gain parameter \( \alpha \) to the feedback loop which is scheduled such that \( \alpha > 0.5 \) for initial iterations to correct for large discrepancies and can be decreased as the improvement between iterations stagnates in order to impart more finely-tuned corrections. Thus, \( \tilde{T}_{i+1} \) becomes \( \tilde{T}_{i+1} = \tilde{T}_1 + aD_i \) where \( \alpha \) is empirically optimized and typically ranges from 0.3 to 0.6 for later iterations depending on the pattern.

We test the feedback algorithm on a variety of patterns of interest, including a ring with a restriction, a Gaussian double-well and various arrays of discrete spots. A summary of the improvements to these optical traps due to the feedback process, along with the number of iterations required \((i)\) and the light-usage efficiency \((\Gamma)\), can be found in table 1. After few iterations of the feedback loop, the measured light profiles shown in figure 2 (continuous light patterns) and figure 3 (discrete spot patterns) show increased accuracy and more closely resemble their target patterns.

As an evaluation metric we use the RMS error,

\[
\epsilon_i = \frac{1}{N_{MR}} \sum_{M_{R}} (M_i - \tilde{T}_i)^2 ,
\]

where \( N_{MR} \) denotes the number of pixels in the measure region. In real optical traps, atoms at temperatures higher than 10% of the trap depth will quickly evaporate from the trap [19]. Following this, we also include the RMS error \( \epsilon^{(10\%)} \) of only those pixels within 10% of the brightest pixel—the trapping minimum—as another figure of merit. Finally, light-usage efficiencies \( \Gamma \) have been calculated for each of the final output patterns. Around 50% of the light incident on the SLM in our experimental set-up is diffracted into the first-order and goes on to make up the hologram (signal and noise regions). To find the overall trap efficiency, we multiply the efficiency of the hologram (the percentage of first-order light in the signal region) with the 50% SLM efficiency.
The measured signal-region intensity for the indented ring is shown in figure 2(a). The main deviation in the initial output is a left-right intensity gradient due to the reduced diffraction efficiency of the SLM at larger deflection angles. This initial pattern has $\epsilon = 21.9\%$, and $\epsilon^{(10\%)} = 9.8\%$. The feedback process corrects for this intensity gradient and also corrects the width of the ring, improving $\epsilon$ to 6.7% and $\epsilon^{(10\%)}$ to 2.1%. Along the circumference, large fluctuations have been suppressed by the feedback process as shown in the plot in figure 2(a). A stagnation point is reached after eight iterations of the feedback loop, as plotted in figure 2(b). In this example the value of $\alpha$ changes from 0.6 to 0.3 after the third iteration. This evolution of the RMS error is typical for most of our feedback optimizations, showing a major improvement in the first iteration, followed by smaller improvements converging to a more accurate pattern. Most patterns are optimized in fewer than ten iterations of feedback, which takes around 10 min to complete. The final optimized phase pattern is saved for future use in cold atoms experiments.

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The final value of $\epsilon^{(10\%)}$ is sufficiently low for experiments of interest in this atom ring-trap. If a ring with 80 $\mu$m radius and 12 $\mu$m width is generated with 3.5 mW of laser power, the trap depth is 69 nK. If a Bose–Einstein condensate of $10^5$ $^{87}$Rb atoms is trapped in this ring at zero magnetic field, the chemical potential is sufficiently low ($\mu = 6.9$ nK) for the atoms to be confined. In particular, this trap can be used for studies of superfluid effects; fluctuations of 2.1% in the trap depth are smaller than $\mu/5$, which is sufficiently low that the superfluidity of the gas persists [20]. This ring pattern may be used to study transport phenomena [21], while indented rings have also been suggested for the study of sonic black hole analogs in atomic condensates [22, 23].

Figure 2. Continuous patterns optimized by feedback. (a) A ring pattern with a Gaussian radial distribution and a restriction (as in figure 1), showing the measured signal region intensity using the initial MRAF-calculated phase profile (left) and after eight iterations of feedback optimization (right), which improve $\epsilon^{(10\%)}$ from 9.8% to 2.1%. (Below) the intensity around the circumference showing the target pattern (red), and the measured profile before (green) and after (blue) feedback. (b) RMS error progression for the ring pattern, recorded at each step of the feedback algorithm. (c) A Gaussian double well, showing signal-region intensity before (left) and after (right) feedback. (Below) a cut across the centre of the two wells, showing normalized intensity for the initial, final and target patterns. For this pattern, $\epsilon^{(10\%)}$ improved from 5.5% to 0.7% within ten iterations.

Figure 3. Discrete patterns. Signal region intensity of (a) a 10 × 10 square lattice and (b) a 16-spot ring lattice before (left) and after (right) feedback. Errors in the trapping minimum decrease from 3.6% to 2.3% for the square lattice and from 2.5% to 1.1% for the ring lattice.
A pattern which particularly demonstrates the robustness of the algorithm is the Gaussian double well shown in figure 2(c), which has many uses for investigating fundamental quantum mechanics [24]. Before feedback the initial output is aberrated to the extent that it resembles a single-well potential. After ten iterations (during which $\alpha$ is fixed at 0.6) the two wells are clearly distinguishable.

In figure 3 the target patterns are different arrangements of simple Gaussian spots of the same intensity. The simple square array is analogous to an optical lattice with the underlying spatially-varying potential removed, while the ring lattice is an experimental geometry which is interesting for quantum simulation [25, 26], but which cannot be created using more conventional methods such as standing waves. Our feedback algorithm corrects the size and position of aberrated spots within ten iterations. We measure a decrease in $\epsilon$ from 22.0% to 15.3% for the square lattice, and from 13.7% to 10.0% for the ring lattice, while $\epsilon^{(105)}$ is reduced from 3.6% to 2.3% for the square lattice, and from 2.5% to 1.1% for the ring lattice.

Experimental optimizations of holographic optical traps have previously been performed for discrete [14] and continuous geometries [13] by carefully characterizing the optical system (e.g. using a Shack–Hartmann wavefront sensor) before applying active feedback. By comparison, such careful characterization is not required with our algorithm. Moreover, our algorithm is sufficiently general to be applicable to both discrete and continuous patterns. The optimization in [14] considers only the height of distinct spots of light, quoting an improved standard deviation of these heights from 19% to 1.4%. Our algorithm corrects also the position and shape of the spots. For comparison, we measure the standard deviation of heights for the ring (square) lattice spots and find an improvement from 20.3% to 1.3% (12.5% to 2.1%). The optimization of continuous light distributions performed in [13] gives light patterns with $\epsilon$ between 6% and 9%, which is again comparable to the values we achieve for the indented ring and double well (6.7% and 5.5% respectively).

In summary, the feedback algorithm is sufficiently robust to correct for large aberrations in the experimentally generated optical traps within few iterations, bringing optical trap discrepancies to the percent level. However, we note that it is important to use the feedback method in conjunction with a hologram–calculation algorithm that suppresses optical vortices at the outset. This is because the feedback is less effective at correcting defects at small length-scales. The MRAF algorithm used here is appropriate with well-chosen initial conditions, while the recently–proposed Conjugate Gradient optimization algorithm [27] is also suitable, and we have already performed initial tests of the compatibility of feedback with Conjugate Gradient optimization, with promising results.

Improvements may be made to the feedback algorithm upon its integration into a cold atoms experiment. The sensitivity of cold atoms to any trapping potential roughness means that we envisage continuing to use the feedback loop by taking in situ images of the trapped atoms [5, 28] rather than directly imaging the light profile. Furthermore, recent developments of high numerical aperture microscope objectives for cold atoms [3, 29–32] could be combined with our approach to produce more finely detailed traps, although this may require more sophisticated calculation stages such as those performed in [33].

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References

[1] Houston N, Riis E and Arnold A S 2008 J. Phys. B: At. Mol. Opt. Phys. 41 211001
[2] Henderson K, Ryu C, MacCormick C and Bosher M G 2009 New J. Phys. 11 043030
[3] Zimmermann B, Müller T, Meineke J, Esslinger T and Moritz H 2011 New J. Phys. 13 043007
[4] Trypogeorgos D, Harte T, Bonnin A and Foot C 2013 Opt. Express 21 24837–46
[5] Muldood C, Brandt L, Dong J, Stuart D, Brainis E, Himsworth M and Kuhn A 2012 New J. Phys. 14 073051
[6] Lee J G and Hill W T III 2014 Rev. Sci. Instrum. 85 103106
[7] McGloin D, Spalding G, Melville H, Sibbett W and Dholakia K 2003 Opt. Express 11 158–66
[8] Bergamini S, Darquie B, Jones M, Jacobowiez L, Browaeys A and Grangier P 2004 J. Opt. Soc. Am. B 21 1889–94
[9] Boyer V, Godun R M, Smirne G, Cassettari D, Chandrashekar C M, Deb A B, Laczik Z J and Foot C J 2006 Phys. Rev. A 73 031402
[10] Franke-Arnold S, Leach J, Padgett M J, Lembessis V E, Ellinas D, Wright A J, Girkin J M, Öhberg P and Arnold A S 2007 Opt. Express 15 8619–25
[11] Bruce G D, Mayoh J, Smirne G, Tarralo-Campo L and Cassettari D 2011 Phys. Scr. T 143 014008
[12] Bruce G D, Bromley S L, Smirne G, Tarralo-Campo L and Cassettari D 2011 Phys. Rev. A 84 053410
[13] Gaunt A L and Hadzibabic Z 2012 Sci. Rep. 2 721
[14] Nogrette F, Labuhn H, Ravets S, Barredo D, Béguin L, Vernier A, Lahaye T and Browaeys A 2014 Phys. Rev. X 4 021034
[15] Bowman D, Ireland P, Bruce G D and Cassettari D 2015 Opt. Express 23 8365–72
[16] Pasienski M and DeMarco B 2008 Opt. Express 16 2176–90
[17] Fortagh J, Ott H, Kraft S, Günther A and Zimmermann C 2002 Phys. Rev. A 66 041604
[18] Gerchberg R W and Saxton W O 1972 Optik 35 237–46
[19] O’Hara K M, Gehm M E, Granade S R and Thomas J E 2001 Phys. Rev. A 64 051403
[20] Ryu C, Andersen M F, Cladé P, Natarajan V, Helmerson K and Phillips W D 2007 Phys. Rev. Lett. 99 260401
[21] Brantut J-P, Meineke J, Stadler D, Krinner S and Esslinger T 2012 Science 337 1069–71
[22] Garay L J, Anglin J R, Cirac J I and Zoller P 2000 Phys. Rev. Lett. 85 4643–7
[23] Garay L J, Anglin J R, Cirac J I and Zoller P 2001 Phys. Rev. A 63 023611
[24] Milburn G J, Corney J, Wright E M and Walls D F 1997 Phys. Rev. A 55 4318–24
[25] Olmos B and Lesanovsky I 2011 Phys. Chem. Chem. Phys. 13 4208–19
[26] Kaminishi E, Kanamoto R, Sato J and Deguchi T 2011 Phys. Rev. A 83 031601
[27] Harte T, Bruce G D, Keeling J and Cassettari D 2014 Opt. Express 22 26548–58
[28] Andrews M R, Mewes M-O, van Druten N J, Durfee D S, Kurn D M and Ketterle W 1996 Science 273 84–87
[29] Alt W 2002 Optik 113 142–4
[30] Bakr W S, Gillen J I, Peng A, Fölling S and Greiner M 2009 Nature 462 74–77
[31] Sherson J F, Weitenberg C, Endres M, Cheneau M, Bloch I and Kuhr S 2010 Nature 467 68–72
[32] Haller E, Hudson J, Kelly A, Cotta D A, Peaudecerf B, Bruce G D and Kuhr S 2015 Single-atom imaging of fermions in a quantum-gas microscope (arXiv:1503.02005)
[33] Lin J, Rodríguez-Herrera O G, Kenny F, Lara D and Dainty J C 2012 Opt. Express 20 1060–9