Measurement of the dependence of ultra diluted gas transmittance on the size of the detector

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We show that measured optical transmittance of an ultra thin gas depends on the detector size. To this end we conducted an experiment that compares transmittances measured in parallel with a pair of detectors with different diameters ranging from 2 to 200 µm. A Tunable Diode Laser Absorption Spectroscopy type system was used. Transmittance of $\sim 10^{-2}$ mbar water vapor on NIR absorption line $\lambda = 1368.60$ nm was measured using a 61.6 m long multi-pass cell placed inside the $\sim 300$ l vacuum chamber. The result of the experiment shows higher transmittances when the measurement is performed using smaller detectors. The difference reaches as much as $1.23 \pm 0.1\%$, which is greater than 0 with $> 5\sigma$ statistical significance. Qualitatively it is in agreement with the recently developed model of thin gas optical transmittance taking into account the quantum mechanical effects of spreading of the wave functions of individual gas particles.

The Beer-Lambert exponential transmission law describing attenuation of monochromatic light by the homogeneous, not very dense medium is well known for almost three centuries. Despite developing newer, more advanced transmittance models, today it still applies to quantitative spectroscopy and rarefied gases, among others. All this models relies on an assumption of attenuating particles locality. However, an increasing number of experiments convince us that the underlying theory of Quantum mechanics is not a local realistic theory. There is one more assumption in most of “classic” transmittance models: a light detector is a macroscopic apparatus. Quantum mechanics is considered to be one of the most fundamental theories so it is necessary to check whether these two assumptions limit scope of applicability of classic models.

Quantum spreading is an effect that involves spatial smearing of the $\Psi$ wave function over time. It leads to the spreading of the $|\Psi|^2$ density of the probability of any reaction (quantum measurement) of a physical object described by such a function. It is derived from solving the Schrödinger equation for a free particle. We applied this solution to each gas particle independently during its free time between successive collisions. It is a kind of “smeared gas”. It leads, together with the assumption of non-locality, to a new model of electromagnetic transmittance of thin gases. One of the predictions of this model is that the measured optical transmittance depends, among others, on the size of the detector used and the duration of the particles mean free time. The classical, “local” approach to transmittance, the Beer-Lambert law included, does not predict any of such dependencies.

Currently, one of the most popular methods of quantitative testing the transmittance of thin gases is Tunable Diode Laser Absorption Spectroscopy (TDLAS). Our setup is a slightly modified version of such a system. The transmittance is measured simultaneously using a pair of detectors with different effective active cross-sections. One laser beam passes through the gas and eventually it’s split towards two detectors with a beam-splitter. There is a big vacuum chamber used to provide conditions for a significant spreading of the gas particles wave functions to occur. The model applies to any type of gas. We chose to test the water vapor.

The objective of the experiment is to examine the qualitative prediction on whether the transmittance measured with a smaller detector is greater than the transmittance measured with a larger detector. Results of the experiment confirm this with $> 5\sigma$ statistical significance.

The experimental setup is described in the next section. The way data is acquired and processed is covered in the following sections. Results are discussed in the 5th section. Conclusions are presented at the end of the paper. The measurement uncertainty is analyzed in the appendix next to the online data guide.

**Experiment Setup.** The schematic diagram is shown in Fig. 1. The tested gas, along with the optical setup and the detectors, is placed inside a bell-type vertical cylindrical vacuum chamber ($a \approx 58$ cm, $h \approx 110$ cm) in room temperature. The working pressure is approx. $10^{-3} - 10^{-2}$ mbar. A DFB SM-pigtailed laser diode (LD-PD Inc., PL-
DFB-1368-A-A81-SA) operating at ∼ 1368.60 nm with 2 MHz line width is used to scan 101313–00021211 water absorption line. The DFB CW output power is about 1 mW at 27 °C. The laser diode is equipped with an internal InGaAs photodiode. The DFB diode is controlled by an integrated current and temperature controller (Thorlabs, CLD1015) placed outside the chamber. The temperature setting of the diode is set to 27 °C. The laser beam is fed into the chamber using single-mode optical fibers (SMF-28E and SMG652.D) using vacuum feedthrough (SQS, KF40 SM). The beam is collimated with adjustable ECO-550 lenses (Thorlabs, PAF2-2C). The vertical multi-pass setup is made up of two 3” dielectric concave mirrors f = 500 mm (Thorlabs, CM750-500-E04-SP) held vertically by metal rods about 76.7 cm apart from each other. Two flat silver mirrors (Thorlabs, MRA03-P01, MRA10-P01) are used to direct laser beam from the collimator to/from the multipass cell and towards a 92/8 pellicle beamsplitter (Thorlabs, CM1-BP108). The first flat mirror that directs the laser beam up to the multipass cell is approx. 8 cm from the collimator. The beamsplitter is approx. 20 cm away from this mirror. Detector 1 is approx. 5.2 cm from the beamsplitter, Detector 2 is 6.7 cm away. The total light path length is approx. 61.4 m long and it is ∼ 1.5 cm shorter towards Detector 1. The multipass cell axis is in line with the chamber vertical axis to assure equally long distance from the chamber walls, approx. 25 cm. All optical components are installed on a small breadboard standing on the chamber floor, see Fig. 2.

Transmittance is measured in parallel by a pair of ø200 µm InGaAs photodiodes (Hamamatsu G11193-02R). A circular aperture stop to reduce detector’s effective active area is inserted in front of the detector (Ch1) placed in line with the beamsplitter incoming beam, see Table 1. The aperture is installed ∼ 1 mm away from the photosensitive surface. The second detector (Ch2), without an aperture, gives a reference transmittance reading. Both detectors and the aperture stop are installed in their own X–Y translation units. The ∼ 92% of the beam is directed towards the first detector.

Both photodiodes operate in a photovoltaic mode with no bias voltage. The photodiode current is amplified by a custom-built current-to-voltage amplifier using the low current op-amp (TI, LMC662), followed by a

Figure 1. The schematic diagram of the experimental setup. All optics and detectors are placed inside the vacuum chamber. The electronic equipment and the laser are kept outside.

Figure 2. A picture of optics in the open chamber.
low-pass 10 Hz RC filter. The amplifier gain is controlled by a feedback loop resistor. The $\text{CH}_1$ resistance is adjusted for each aperture individually to keep output voltage within a range of a few dozen mV, see Table 1. The $\text{CH}_2$ resistance is constant and equal to 2k$\Omega$. Gains are chosen to obtain both characteristics curves as linear as possible within the range used for actual measurement.

Vacuum is evacuated with a scroll pump and a turbo molecular pump. Two independent vacuum meters are used (Leybold, Ceravac CTR 100N, Ionivac ITR90).

All voltage data is acquired by the DAQ unit (LabJack, U6). The digital data, from the DAQ unit and the laser driver, is retrieved via a USB by a PC computer running LabView. A custom built LabView GUI is used to automate the measurement procedure. The LabView text files data is extracted periodically into the SQL database from where it is retrieved for statistical analyses performed by the Mathematica 12 package.

In this paper $\text{CH}_1$ and $\text{CH}_2$ may denote either a respective photodiode or one of measurement channels or a voltage read from one of channels.

**Gas and spectral line selection.** We selected water vapor due to its large cross-section in the near infrared. The HITRAN$^{14}$ and MARVEL$^{15}$ data was referenced. The large cross-section allows for testing transmittance at low pressures with shorter path of light. Low pressure and a narrow spectral range of the laser allow for isolating a single absorption line with sufficient resolution.

For our setup the expected mean free path of water particles for the pressure of $\sim 10^{-3}$ mbar is longer than 37 cm. With approximate mean speed in the room temperature of 600 ms$^{-1}$ it gives approx. 0.6 ms particle mean free time. Plugging this time to the Schrödinger equation free particle solution we calculate the particle wave packet standard deviation to be $\sim 14.6$ µm. This is a conservative calculation using ideal gas laws.

The chamber size is another restriction on the particle mean free path. There should be enough distance between walls and the measuring laser beam. This is why a chamber diameter of 58 cm was chosen.

**Stages of the experiment.** The experiment is carried out in successive, several days long runs, see Table 2. There is a different aperture stop installed during each run. A run consists of many consecutive either 30 min or $\sim 10$ min long cycles.

Replacement of an aperture requires opening of the vacuum chamber. After the aperture installation, the $\text{CH}_1$ gain is adjusted by soldering in the appropriate feedback loop resistor. In case of two runs (R-8 and R-10), the aperture stop was removed in order to perform a comparative measurement for two detectors equal (according to manufacturer) in size.

After the chamber has been closed, vacuum is build to $\sim 10^{-5}$ mbar, which takes roughly 1–2 days. In some cases, the decision was taken to extend this period to 3–5 days. Water is sucked in from an external tank due to water vapor tends to settle on the inside walls of the chamber and setup components$^{16}$. This can be seen in the spontaneous pressure drop, starting immediately after the feed valve has been closed. To obtain the working pressure in the order of $10^{-3} - 10^{-2}$ mbar, the valve is kept open for a longer period of time (e.g., an hour), while maintaining higher pressure (e.g., 2 $\times$ 10$^{-2}$ mbar), see pressure plots in Fig. 9.

The pressure measurement below 10$^{-3}$ mbar, made using the Ionivac vacuum gauge ($\text{PR}_S$), is burdened with quite a large error, in the order of ±15%. However, this range is used solely to build vacuum prior to feeding the water. The total working pressure, i.e. above 10$^{-3}$ mbar, is measured, with the accuracy of ±0.5%, using the Ceravac vacuum gauge ($\text{PR}_A$). The partial pressure of the water ($\text{PR}_W$) may be determined by converting the classical transmittance measured with $\text{CH}_2$, see Eq. 6. The partial pressure can be determined in our setup within the range of approx. 1 $\times$ 10$^{-3} - 3 \times 10^{-2}$ mbar.

To purify the chamber atmosphere vacuum may be build and water may be fed many times during a single run without opening the chamber. These operations are visible as discontinuities on pressure plots in Fig. 9.

### Table 1. $\text{CH}_1$ aperture stops parameters.

| Size | 2 µm | 5 µm | 15 µm | 25 µm | 40 µm | 50 µm | 100 µm | 150 µm |
|------|------|------|-------|-------|-------|-------|--------|--------|
| Model | P2H  | P5D  | P15D  | P25D  | P40D  | P50D  | P100D  | P150D  |
| Diameter tolerance | ±0.25 µm | ±1 µm | ±1.5 µm | ±2 µm | ±3 µm | ±3 µm | ±4 µm | ±6 µm |
| Circularity | ≥85% | >90% | >90% | >95% | >95% | >95% | >95% | >95% |
| Gain - resistor (Ω) | 50 $\times$ 10$^3$ | 10 $\times$ 10$^3$ | 51 $\times$ 10$^3$ | 51 $\times$ 10$^3$ | 51 $\times$ 10$^3$ | 51 $\times$ 10$^3$ | 2 $\times$ 10$^4$ | 2 $\times$ 10$^4$ |

### Table 2. Basic statistics of the experiment runs.

| Run name | R-3 | R-5 | R-6 | R-7 | R-8 | R-10 | R-11 | R-12 | R-13 | R-14 | R-15 |
|----------|-----|-----|-----|-----|-----|------|------|------|------|------|------|
| Aperture installed | 2 µm | 2 µm | 25 µm | 5 µm | none | 150 µm | none | 15 µm | 40 µm | 25 µm | 50 µm | 100 µm |
| No. of cycles | 131 | 218 | 71 | 81 | 31 | 268 | 709 | 558 | 645 | 1177 | 1014 | 1012 |
| No. of measurements | 384 289 | 577 676 | 183 212 | 214 318 | 80 220 | 695 544 | 1 185 491 | 262 717 | 202 953 | 555 846 | 478 307 | 479 172 |
Figure 3. Sample readings of the Ch3 detector during two successive 30 min cycles along with both cycles steps numbers are presented. Reversing laser current step is visible at the 1st step of the second cycle.

Data acquisition
Within a single run the measurement is made in cycles composed of following steps:

1. measuring detectors characteristic curves,
2. tuning in the wavelength of the laser light to the chosen absorption line,
3. measuring both transmittances,
4. measuring detectors characteristic curves again (with the laser current step reversed).

The 4th step is the 1st step of the next cycle. Fig. 3 presents sample readings of the Ch3 detector during two successive cycles. Cycles last either 30 min or (in the 2nd part of the experiment) 10 min. All cyclic measurements are fully automated with a LabView app. Each cycle has its own, time-based identifier assigned e.g., 20200314-0531. The identifier is referred during data post processing and data presentation.

Detector characteristics acquisition (step 1). The setup is susceptible to various types of drifts: laser tuning, changes in light polarization in optical fibers (affecting the detector readings), pressure and mechanical changes. They cause, among others, a change of the detector characteristics. Due to the adopted method of determining the transmittance quotient, acquiring the appropriate voltage versus light power characteristic curves is of key importance: P1 (Ch1) and P2 (Ch2). Although they are called for convenience “detectors characteristics”, they are not just photodiodes characteristics. They cover all light & signal processing steps in turn: the fibers & mirrors light attenuation, the aperture stop (Ch2 only), the photodiodes light-to-current conversion, the current-to-voltage conversion & amplification and A/D conversion.

The characteristics are determined by changing the DFB diode current ILD. Based on the fact that the DFB diode output power is proportional to the current set, the detector response is determined as a function of the laser power. The range of current changes is automatically selected based on the last reading (from the previous cycle) of the transmittance in the absorption line. It is assumed that the transmittance in the current cycle will be similar to the previous one, i.e. that the partial pressure of the water vapor does not change significantly.

The span of the ILD current changes is arbitrarily set as either ΔILD = ±12 mA for 30 min long cycles or ΔILD = ±9 mA for the shorter ones. DFB controller’s minimum current step is 0.05 mA. It is known that a change of the DFB diode current also causes a change of the wavelength. In case of the diode used in the experiment Δλ/ΔILD ≈ 78 pm mA⁻¹, which for (current span of) 24 mA leads to a change of the wavelength by ~ 1.8 nm. We chosen span and range to avoid overlapping with other strong absorption lines while characteristics acquisition.

Such a change in wavelength may also cause a slight change in detector sensitivity (up to 1% according to the manufacturer). It is assumed, however, that due to the use of two detectors from the same series, the relative change in sensitivity between the detectors is the same. The same offset cancels possible measurement error because it appears both in the numerator and the denominator of the formula used to determine the transmittance quotient, see Eq. (3).

It is required that the actual laser temperature is within the ±0.003% range from the set point of 27 °C for each measurement. The scan starts 250 ms after reaching required temperature range. Each recorded measurement within a scan is the arithmetic mean of 30 consecutive single readings (Ch1, Ch2, PLD) made every 11 ms. Despite allowing a fairly narrow range of stabilized temperature, the current change direction (up/down) is switched in each cycle. It’s either +0.05 mA or −0.05 mA. A constant increase (or a decrease, accordingly) of the laser current ILD makes the laser diode working temperature always a little higher (or lower, accordingly) on average. This is because the temperature compensation circuit (Peltier TEC, PID) keeps up with the current changes quite slowly. To compensate for this effect the measurements obtained both at the beginning and at the end of the cycle (steps 1 & 4) are used together to calculate the characteristic curve for the given cycle. This way up to 2 × 2 × 12/0.05 = 960 (or later 2 × 2 × 9/0.05 = 720) points are available for approximate characteristics models.

The scan range may be automatically limited from the bottom. For higher pressures (in the order of 10⁻² mbar) the absorption line is so deep that only a few percent of the light reaches the detectors. In such case the characteristic is obtained close to the lower limit of the laser action and it is impossible to measure some of the distant points in the ΔILD negative range. The measurement of the characteristics is then limited so that the ILD current fed is large enough (min. 3 mA) to excite the laser action.
The scan range is limited from the top as well. Laser current \(I_{LD}\) can’t exceed 52 mA, so that, by accident, no measurement of the water absorption line is made.

The characteristic acquisition takes approx. 6 minutes. Most of this time is spent waiting for temperature stabilization of the laser.

### Tuning in the wavelength (step 2).

After the characteristics has been measured, a fixed value of the laser current \(I_{LD}\) is set to get the wavelength as close as possible to the absorption line maximum. Because of drifts of the diode and the controller it’s necessary to adjust the laser current \(I_{LD}\). We check, for 3 distinct settings, which transmittance in the \(O_2\) detector is the lowest: one that is identical as in the previous cycle or one that is different by either plus or minus 0.05 mA. Checking starts 45 seconds after the measurements of the characteristics had been completed, providing time to properly relax temperature of the laser to the range of \(\pm 0.003\%\). This way, actual wavelength is kept as close as possible to the absorption maximum during the entire experiment.

### The transmittances measurement (step 3).

Having set the fixed laser current and temperature set-points near the absorption line maximum, the transmittances measurement is carried out in the continuous mode. We don’t use any wavelength modulation techniques. Single measurements are recorded twice a second. A single measurement includes following parameters read synchronously: both detectors voltages \((Ch_1, Ch_2)\), laser power read from the laser photodiode \((PLD)\), actual laser temperature and current \((T_{LD}, I_{LD})\) as well as both pressure readings \((PRS_A, PRS_B)\). This measurement step ends half an hour (or 10 min) from the start of the cycle.

### The 2nd characteristics acquisition (step 4).

The last step in the cycle is to acquire measurements for the characteristics again. This time, stepping the laser current in the reverse direction. It is also the first step of the next cycle.

### Data processing

The difference of the water vapor transmittances measured by both detectors is calculated as the transmittance quotient \((TQ)\) according to the following procedure.

#### Determination of the linear model of the detector characteristics.

The characteristics \(P_1(Ch_1)\) and \(P_2(Ch_2)\) of both detectors are determined for each measurement cycle. They are approximated with a linear regression near the range of the detector voltage values observed during the given measurement cycle:

\[
P_1(Ch_1) = A_1 Ch_1 + B_1, \quad P_2(Ch_2) = A_2 Ch_2 + B_2,
\]

where \(A_{1,2}\) and \(B_{1,2}\) are linear model coefficients.

There are up to 960 (or 720) points \((Ch_{1n}, P_{1Ln}),(Ch_{2n}, P_{2Ln})\) available for each linear regression fitting. \(P_{1,2}\) is the power of light emitted by the laser as reported by the DFB built-in photodiode, \(Ch_{1,2}\) is the detector’s voltage reading, the \(n\) index denotes the subsequent readings during scans. See Fig. 4.

A set of points used for actual fitting is limited to the range of voltages measured by the detector within the cycle. It gives linear approximation with a smaller error within the interesting range. Usually these are very narrow ranges of detector operation (e.g. tenths of mV), resulting from noise and a small pressure difference during the cycle. Very often they are so narrow that there are too few measurements available for accurate model fitting. The range is then extended up to 25% of the voltage range of the characteristic being measured. This way the model is fitted using approx. 150–200 points only. Thanks to the surplus of points, the linear regression can be assessed visually in a broader context, see overview in Fig. 4. Such plots are available online for all measurement cycles.

### Figure 4.

Example of linear approximation of both characteristics along with source measurements. The colored vertical stripe indicates the range of the detected voltage variability in the cycle. The grey vertical stripes indicate an additional range (up to 25%) of the points used to determine the linear regression.
Transmittance Quotient calculation. Gas optical transmittance is the ratio of the power of the light beam that has passed through the medium divided by the power of the light that has entered the medium. The characteristics of the detectors calculated above allow for calculating the transmittance for each of the channels:

\[
TR_1 = \frac{P_1(CH_1)}{P_{LD}}, \\
TR_2 = \frac{P_2(CH_2)}{P_{LD}}. 
\]

All "constant" light power loses for both measurement channels are encoded within \(P_1\) and \(P_2\) models, respectively. These losses mainly result from mirrors reflectivity, photodiodes efficiency and beam splitting. This way the Eq. (2) are valid for determining just water vapor transmittance.

We compare transmittance values using the transmittance quotient (TQ) as defined below:

\[
TQ = \frac{TR_1}{TR_2} = \frac{P_1(CH_1)/P_{LD}}{P_2(CH_2)/P_{LD}} = \frac{P_1(CH_1)}{P_2(CH_2)}. 
\]

Note that the quotient defined above is not a simple quotient of light power measured by both detectors. It is the quotient of transmittances measured by both detectors. There is either transmittance difference or transmittance quotient referred in this report. Transmittance difference is expressed as a percentage so it is just the transmittance quotient minus 1. TQ values greater than 1 (transmittance difference greater than 0) mean that the transmittance measured by the smaller detector \(CH_2\) is greater than the transmittance measured by the classical one \(CH_1\). Examples of the TQ values for the individual measurements are shown in Fig. 6.

There is a possible issue with a non linearity of the DFB laser diode (current vs output power) and the DFB photodiode (incident light vs current). It was checked that this non linearity is so small in the operational range that it doesn’t significantly affect transmittance measurement. It should be taken into account for very accurate transmittance measurements. Besides we’re interested just in transmittance quotient in this experiment. This non-linearity cancels out because it appears in both numerator and denominator of Eq. (3).

The actual reading (including its error) of the laser photodiode (\(P_{LD}\)) is irrelevant for the calculation of transmittance quotient TQ because it cancels out appearing in both numerator and denominator of Eq. (3).

Determination of the transmittance and their quotient is possible only if the domains of characteristics \(P_{1,2}\) includes the appropriate range of the \(CH_{1,2}\) voltages. It is checked automatically for each cycle. If the appropriate characteristic range is missing the measurements made within the given cycle are skipped by the aggregating algorithm. It may happen sometimes for sudden pressure changes.

There is a small (\(\sim 1.5 \text{ cm}\)) difference in total light path length towards detectors. Because light path towards Detector 1 is \(\sim 0.024\%\) shorter transmittance measured by Detector 1 is systematically \(\sim 0.024\%\) higher. We will see later that such a difference is negligible but it should be noted.

Transmittance Quotient aggregation. We determine the transmittance quotient for each single measurement within a cycle. There are 2 measurements per second recorded which makes hundreds measurements per cycle. Assuming that the experimental conditions are sufficiently constant during the cycle, the average transmittance quotient \(TQ_k\) for the entire cycle is determined.

Figure 5. Example of the linear regression residuals—only within the range of points designated for determining the regression.
where \( k \)-cycle index, \( M_k \)-number of the single measurements in the \( k \)-th cycle, \( m \)-measurement index within a cycle, \( A_{1,k}, B_{1,k} \)-linear regression factors of \( P_{1,k} \) characteristics, respectively for channel 1 and 2.

Determination of the transmittance quotient \( TQ \) for the entire run (for single aperture) involves calculating the arithmetic mean of the quotients measured in the successive cycles:

\[
TQ = \frac{1}{K} \sum_{k=1}^{K} TQ_k
\]

where \( K \)-number of cycles in a run.

**Water vapor partial pressure calculation.** Having determined the classical transmittance in the \( Ch_2 \) channel, the partial pressure of water vapor (\( PRSH_{2O} \)) can be determined based on the relationship between transmittance, absorbance and pressure:

\[
PRSH_{2O} \approx -0.00854 \log(TR_2) \text{ mbar}.
\]

We calculated the conversion factor depending on light path length, absorption line cross-section and temperature.

**Results and interpretation**

The aggregated results of the experiment are presented in Fig. 7. The mean transmittance quotient \( \overline{TQ} \) is shown for each individual aperture examined. The rightmost point is the result of no aperture runs. All measured values are greater than 100%. It means that the \( Ch_1 \) (smaller) detector measured higher transmittance.

All presented quantitative results (transmittance quotient and transmittance difference) don’t take into account the systematic shift introduced by the \( \sim 0.024\% \) shorter light path towards Detector 1. This is because one may simply shift the reference base from 100% to 100.024% when analyzing if transmittance measured with the smaller detector is greater or not.

The more detailed graphs showing the values of measurements for the individual cycles along with pressure and transmittance are presented in the Appendix, see Fig. 9. Yet more data and figures are available online at [www.smearedgas.org/experiment1](http://www.smearedgas.org/experiment1). Among others, there are “cycle cards” prepared for all measurement cycles. They presents all essential data collected during single cycle along with parameters calculated, see Appendix for the guide. Raw data is available upon request.

**Runs with aperture stops.** We observe that all runs with the pinhole installed show higher transmittance when measured by the smaller \( Ch_1 \) detector! This is exactly the effect qualitatively predicted by the smeared gas theory. For runs with bigger, namely 25-, 40-, 50-, 100- and 150 \( \mu \)m apertures, the statistical significance is higher than 5\( \sigma \).
The maximum transmittance difference equals to 1.23 ± 0.1 %, when the 50 µm aperture is installed. For the 100- and 150 µm apertures the difference is equal to 0.52 ± 0.06 % and 0.53 ± 0.07 % respectively. They are smaller than the 50 µm aperture result. This is in line with the model's qualitative prediction: as the detector size increases, the measured transmittance should decrease—for detectors significantly larger then the wavelength (a kind of geometric optics approximation).

This relationship is the other way around for the 6 smallest apertures, however. Furthermore, for the 3 smallest apertures the statistical significance falls down to 2–3σ. This is because the transmittance, according to the smeared gas model, is proportional to the definite integral of |Ψ|^2 over so-called "visibility tunnel". The visibility tunnel is a volume where a photon amplitude doesn't cancel out when using certain detector - according to the path integrals approach. For detectors comparable in size to the wavelength the non-cancelling photon probability amplitudes outside the "classic" visibility tunnel effectively thicken this tunnel. This increases the volume over which the probability distributions of the smeared gas particles are integrated. As a consequence, the likelihood of observing a photon scattering event with such a small detector rises. Therefore, the measured transmittance decreases—in the extreme case down to the classical transmittance level. We see this kind of relation on the left side of the Fig. 7. The transmittance quotient is decreasing towards 100% along with decreasing Ch1 detector aperture diameter (from 50- down to 2 µm).

The result for the 100 µm aperture (with much higher average pressure) is discussed later on. The very low reading for the 15 µm aperture needs further analysis.

The quantitative model fitting to experimental results will be performed further down the line. Still, we observe qualitative predictions are met in the experiment.

Control runs without aperture. During the R-8 and R-10 runs there are no apertures installed. Transmittance is measured using two naked detectors with a comparable diameter. The measured transmittance difference is 0.12 ± 0.04 %. The transmittances are thus not perfectly identical but very close to each other.

Apart from obvious measurement errors, such difference may result, for example, from the diameter tolerance due to the workmanship of the detectors themselves, impurities etc. This tolerance, in turn, is irrelevant in case of the measurements made with aperture stops in place because detector Ch1 is obscured by the aperture anyway. Another reason for the observed difference may be a potential variance in the sensitivity of both detectors to different wavelengths as discussed earlier. This may cause some systematic error when determining the characteristics of all measurements. However, this control runs would indicate at least the order of magnitude of such a systematic error. Even if it is ~0.12 %, it is still significantly smaller than the measured transmittance differences for 5 apertures larger than 25 µm. Consequently, it does not undermine the conclusions drawn.

Transmittance quotient versus pressure. There are at least two phenomena influencing the transmittance quotient that should be taken into account when the pressure changes and temperature is kept constant. As the pressure increases, (1) the number of molecules increases (the transmittance drops), (2) the mean free path shortens. The experiment was not designed to examine these correlations so very little may be concluded in this field. However, there are some indications we can take a closer look at. They are in accordance with the model.

Transmittance quotient versus number of molecules. According to the model the increasing number of molecules with the mean wave function spread unchanged (aka the mean free time constant) along with a fixed visibility tunnel should increase the transmittance quotient. We show it qualitatively on the Fig. 8. There are presented sample predictions of the model in a range of "geometric optics" approximation for two different water vapor partial pressures: ∼ 1 × 10^{-2} mbar and ∼ 6 × 10^{-3} mbar. According to Eq. (6) they correspond to
transmittance \((TR_d)\) of 30\% and 50\% respectively. The transmittances for each detector \(d = 1, 2\) are calculated with the following equation\(^9\):

\[
TR_d(l) = \prod_{n=1}^{N} \left(1 - \frac{G_d(l)}{4} \left[ \text{erf} \left( \frac{\sigma_n - rTd}{\sqrt{2}\text{stdev}_A(l)} \right) - \text{erf} \left( \frac{\sigma_n + rTd}{\sqrt{2}\text{stdev}_A(l)} \right) \right]^2 \right),
\]

(7)

where \(\bar{t}\) denotes the molecules mean free time, \(N\) is a number of molecules in the chamber, \(\sigma_n\) is the \(n\)-th molecule distance from the beam. The standard deviation \(\text{stdev}_A(l)\) is assumed to be \(\sim 14.6 \, \mu\text{m}\) (see next paragraphs). The geometry coefficient \(G_d(l)\) is equal to cross section of the 101313-000212\(^{11}\) water absorption line (\(\approx 7.76 \times 10^{-19} \, \text{cm}^2\)) divided by the area of the detector. Theoretical transmittance quotients are calculated assuming the transmittance tunnel has the shape of a 60 m long truncated cone. The smaller base is of the size of an aperture. The angle (an effective divergence towards the source) is 0.008 mrad. Note, that this divergence is much smaller than the typical laser beam divergence thanks to the spherical mirrors re-focusing the beam for 80 times. The \(rTd\) is the radius of the (cylindrical) visibility tunnel, it’s different for each detector \(d\). For simplifying calculations the conical tunnel is approximated as a cylinder, thus \(rTd\) is equal to the mean of both bases radii.

There are \(TQ\) measurements shown on the Fig. 8 for at least 4 different apertures: 25-, 40-, 50- and 150 \(\mu\text{m}\) following the model qualitative prediction: \(TQ\) is higher for the higher pressure. The statistical significance of this relation reaches as much as 3\(\sigma\) for the 25- and 40 \(\mu\text{m}\) apertures. Measurements for other apertures and pressures are omitted due to missing comparable data.

### Transmittance quotient versus mean free path.

The measured transmittance quotient for the 100 \(\mu\text{m}\) aperture stop is smaller than ones measured for 50- and 150 \(\mu\text{m}\) apertures, see Fig. 7. According to the model \(TQ\) closer to 100\% may indicate a shorter mean free time. Indeed for the 100 \(\mu\text{m}\) aperture stop, most of the time the total pressure was higher than \(3 \times 10^{-2}\) mbar and the water vapor partial pressure \(\text{PRSH}_{1,0}\) was higher than \(1 \times 10^{-7}\) mbar. The measurements for other apertures was made at a lower total pressure, approx. in a range from \(1 \times 10^{-3}\) mbar to \(3 \times 10^{-2}\) mbar. It seems that so high pressure eventually led to shortening the mean free path to a value smaller than the one constrained by the chamber size. This way the water molecule wave function standard deviation might drop below 14.6 \(\mu\text{m}\) lowering the \(TQ\) reading.

### Further works

First of all it is necessary to conduct the quantitative model fitting. Careful consideration of the shape of the visibility tunnel is essential. All factors like reflections, collimation, laser power density or small apertures (non-classic trajectories) should be taken into account.

The experiment should be repeated under modified conditions to eliminate any missed systematic errors and increase accuracy. Potential modifications include, among others:

- making both light paths equal in length,
- analyzing and/or avoiding interference caused by the single mode laser (fringes),
- a split of the beam in parallel towards more than 2 detectors,
- mounting apertures at each detector and testing the differences under varying configurations of reflection and beam split, e.g., 50/50 split,
better ways to reduce diode noise, e.g., changing the wiring or moving the first stage amplifiers closer to photodiodes, even inside the vacuum chamber,
more precise tuning of the wavelength to the absorption line using externally modulated laser driver, controlled with the standalone wavemeter or the lock-in feedback loop\textsuperscript{4},
increasing the diameter of the vacuum chamber (extending the mean free path),
more stable fastening of the multi-pass cell mirrors,
removing the multi-pass cell rods shortening the mean free path near the laser beam,
applying a different number of reflections in the multi-pass cell,
assembling the measuring system outside the main section of the vacuum chamber so that the system could be reconfigured faster,
testing other gases e.g., methane (also with a large cross section in NIR).

A slight modification of the proposed method will allow for conducting measurements of transmittance differences and mean free paths for larger working pressure ranges. In particular, the length of the light path should be adjusted by controlling the number of reflections in the multi-pass cell. The experiment can be carried out without the use of a multi-pass cell, using a sufficiently long vacuum chamber.

Another modification may involve enabling limiting and adjusting the mean free path by installing internal walls or pipes. This will allow for studying the relationship between the transmittance quotient and the mean free path.

The presented values of the transmittance quotient in a range of 1% may not seem respectable. However, higher values can be achieved e.g., by lengthen particles mean free time in a bigger chamber.

Conclusions
For ultra thin gas we observed the effect of changing the optical transmittance measurement readings using detectors of different sizes. For detectors of a diameter much bigger than the wavelength transmittance increased as detector size decreased. Thus, the objective of the experiment, which is to observe in laboratory conditions the qualitative effect predicted by the non-local smeared gas transmittance model\textsuperscript{9}, is achieved. The fact of observing a non-obvious phenomenon predicted by the theory is a strong premise for its validity. As far as we know there is no other gas transmittance model predicting such results.

The results are presented with a very high statistical significance level thanks to the long, repetitive measurement process. However, too few measurements were made to categorically determine the type of relationship between transmittance quotient and pressure. Moreover, there are many other improvements available regarding robustness, accuracy, flexibility etc. Some of them are outlined in the paper.

This experiment is a kind of a typical quantitative spectroscopy setup. It is relatively cheap and easy to repeat. However, it differs in two very important details from a well known TDLAS. Firstly, a sufficiently long gas particles mean free path is required. Free from any reactions that could be considered a quantum measurement or lead to decoherence. Therefore, the following should be provided: a large chamber, low pressure, electromagnetic shielding and weak measurement laser light. Secondly, the detector’s light sensitive diameter should be comparable (or lower) to the standard deviation of the smearing of the tested gas particles wave packets. It seems highly unlikely that both of these conditions could have been accidentally met during some earlier quantitative spectroscopy experiment. No reports of a similar experiment have been found in the literature.

In the experiment quite small detectors where used and a moderate pressure with a not so long light path was examined. However, the shown predictions of the smeared gas model apply for lower pressure levels, bigger detectors and longer distances. We believe the suitability of the smeared gas’ model should be verified in relation to the conditions of astronomical measurements.

Appendix
Cycle measurement results. There are measurement results for each cycle presented in Fig. 9. They are grouped by the $\text{CH}_2$ aperture size, aggregating data from different runs if required. Each point on a plot represents the measurement result for an entire (either 10- or 30-minutes long) cycle. The graphs also present bands showing the $\sigma_1$ and $\sigma_5$ measurement uncertainties accumulated for the preceding cycles. There are both total & partial pressure and transmittance plots superimposed. Single measurements results are available online.

Online data. Online data & additional material are available on the website https://www.smearedgas.org/experiment1. There is a separate web page for each aperture size available. It consists of a run (or runs) summary, timeline figures and a list of measurement cycles within those runs. For each cycle on the list there is a link to a “cycle card”. All single measurements taken during a cycle are shown on a single cycle card. A sample cycle card is presented in Fig. 10. It consists of the following sections.

1. The title of the card includes id of the cycle, the aperture diameter, the run name, timestamp the cycle started and the mean transmittance quotient (TQ) as measured in the cycle.
2. The timeline of the cycle contains the total & partial pressures (red, dashed) and power of light (blue) as detected by the reference ($\text{CH}_2$) detector. The partial pressure is calculated only for the period during which the transmittance measurement was carried out (the 3rd step of a cycle). The total pressure shown is measured with the PRSA vacuum meter.
3. The linear approximation of the $\text{CH}_1$ characteristic along with source measurements. The colored vertical stripe indicates the range of the detected $\text{CH}_1$ voltage variability during the cycle. The grey vertical stripes indicate an additional range (up to 25%) of the points used to determine the regression. The triangle direc-
Figure 9. Mean transmittance quotients along with their 1σ standard errors for the individual cycles and the bands showing the accumulated 1σ and 5σ measurement uncertainties, both total & partial pressures and transmittance readings are superimposed.
tion reflects the laser current stepping direction during scanning (the 1st & 4th steps of a cycle). Refer to Fig. 4 notes in the main text for more details.

4. The same as the #3 above but for the $Ch_2$ detector.
5. The $Ch_1$ linear regression residuals - within the range of points designated for determining the regression.
6. The same as the #5 above but for the $Ch_2$ detector.
7. The timeline contains each single reading of the $Ch_1$ detector recorded. The left axis presents raw voltage as reported by the DAQ unit. On the right axis there is the corresponding power of light as calculated with the current cycle's $P_1$ characteristic model. The dashed horizontal lines denote the mean value and ±1σ deviation.
8. The same as the #7 above but for the $Ch_2$ detector.
9. Each point is the transmittance quotient $TQ_{m}$ calculated for a pair of $Ch_{1m}$ & $Ch_{2m}$ values from the same measurement. The dashed horizontal lines denote the mean value, its standard deviation and the standard error of the entire cycle.
10. A variety of the run and cycle parameters.
11. The parameters of both $P_1$ & $P_2$ characteristics models determined in the cycle.
Figure 10. All measurements taken during the cycle are shown on a sample cycle card. The numbers in the circles refer to the sections descriptions in the text.
12. The mean transmittance quotient for the cycle (referred as \( \overline{TQ_k} \) in the main text) along with its standard error and other uncertainty related parameters: the number of measurements, the mean detector readings and the relevant standard deviations.

13. The footer contains the software version used & card generation timestamp.

**Uncertainty and errors.** Two main areas where errors originate can be distinguished in the system: i) errors in determining the characteristics of the detectors and ii) errors while performing the actual measurement of the transmittance i.e., power of light received by the detectors. The error in determining the characteristic is a systematic error in measuring the transmittance quotient in the given cycle. When aggregating data from multiple cycles, this error becomes a random error, however. Therefore, the rules used to calculate the standard error of the mean can be applied. Transmittance measurement errors are always random errors.

Although the setup remains unchanged all the time, the measurement error is different for the runs carried out with different apertures. This is due to the fact that for the individual apertures detector \( Ch_1 \) works at different parts of its characteristic. In particular, in case of small apertures of 2 \( \mu \)m & 5 \( \mu \)m the detector works close to the lower limit of its sensitivity and therefore its signal to noise ratio is lower. In addition, various gains are used in channel \( Ch_1 \).

Furthermore, values of transmittance itself vary, as it depends, after all, on the partial pressure of the water vapor in the chamber. Error rate also depends on the wiring. The result is that the partial derivatives used to calculate error propagation in each cycle may vary. As a consequence, errors has to be estimated for each cycle independently.

The measure of uncertainty in the experiment is standard deviation and standard error. We use typical uncertainty propagation rules based on partial derivatives for their calculation\(^9\).

Equation (4) let us determine standard error \( \sigma TQ_k \) of the mean transmittance quotient in the \( k \)-th cycle:

\[
(\sigma TQ_k)^2 = \sum_{d=1}^{2} \left( \frac{\sigma A_{dk}}{P_{dk} A_{dk}} \right)^2 + \frac{1}{N_k} \left( \frac{\sigma Ch_{dk}}{P_{dk} Ch_{dk}} \right)^2 + \left( \frac{\sigma B_{dk}}{P_{dk}} \right)^2,
\]

where aggregation based on \( d = 1, 2 \) denotes both detectors’ errors. Parameters \( \sigma A_{dk} \) and \( \sigma B_{dk} \) denote standard deviations of parameters \( A_{dk} \) and \( B_{dk} \) of the characteristics models of detector \( d \) in the \( k \)-th cycle. These deviations are calculated when linear regressions of characteristics \( P_1(Ch_1) \) and \( P_2(Ch_2) \) are determined.

There are some approximations applied in Eq. (8). They are based on the fact that throughout the entire cycle the \( Ch_{dm} \) readings are relatively constant and approximately equal to the cycle’s mean \( Ch_{dk} \):

\[
\overline{Ch_{dk}} = \frac{1}{M_k} \sum_{m=1}^{M_k} Ch_{dm}.
\]

Therefore \( P_{dk}(Ch_{dm}) \) can be approximated with \( P_{dk}(\overline{Ch_{dk}}) \), an average independent of \( n \):

\[
P_{dk} = P_{dk}(\overline{Ch_{dk}}).
\]

We also disregard the variability of \( \sigma Ch_{dm}/Ch_{dm} \) for the successive measurements due to the low variability of the denominator. The \( \sigma Ch_{dk}/Ch_{dk} \) quotient is used instead, where \( \sigma Ch_{dk} \) denotes the standard deviation of the measurements in detector \( Ch_1 \) during the \( k \)-th cycle.

The \( Ch_{dm} \) value may drift due to small pressure drift during the cycle. Usually it will be a small, continuous change due to a small continuous change of the partial pressure of water vapor. This drift has nothing to do with the measurement error and could be compensated (with a kind of trend detection) when determining the standard deviation induced by real random errors. However, we don’t compensate this trend what leads to a bit higher uncertainty. It’s a conservative approach. It makes algorithm simpler and actually there is not so many cycles with high pressure drifts. It should be noted that the drift has no effect on the measurement of the transmittance quotient, since the quotient is calculated individually for each \( n \)-th measurement within a cycle.

In order to determine standard error \( \sigma TQ \) for the entire measurement run we use the formula:

\[
\sigma TQ = \sqrt{\frac{1}{K} \sum_{k=1}^{K} (\sigma TQ_k)^2},
\]

Preliminary analysis indicates following sources of noise during the experiment.

1. Own noise of photodiodes operating at very low light with a significant dark current input.
2. Electromagnetic interference by photodiodes wiring.
3. Photodiodes and wiring noise amplification by both amplifier stages.
4. Pendulum type vibrations of the upper mirror of the multi-pass cell amplified by the multiple reflections of the laser beam.
5. Laser light power and wavelength drift caused by laser current and operating temperature drifts.
6. Changes in polarization and/or intensity of light incident on the detectors resulting from optical fiber tension and vibrations.
7. Variable interference patterns (fringes) of a single mode laser light caused by (i) changing wavelength during characteristics determination, (ii) mechanical drifts. This is a very low frequency noise or even a potential systematic error.

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