Numerical Analysis to Determine Reliable One-Diode Model Parameters for Perovskite Solar Cells

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Abstract: With the aim to determine the photo-generated current, diode saturation current, ideality factor, shunt, and series resistances related to the one-diode model for p-i-n planar perovskite solar cells, reference cells with active area of approximately 1 cm² and efficiencies ranging between 4.6 and 12.2% were fabricated and characterized at standard test conditions. To estimated feasible parameters, the mean square error between the I-V curve data of these cells and the circuital model results were minimized using a Genetic Algorithm combined with the Nelder-Mead method. When considering the optimization process solutions, a numerical sensitivity analysis of the error as a function of the estimated parameters was carried out. Based on the errors behavior that is showed graphically through maps, it was demonstrated that the set of parameters estimated for each cell were reliable, meaningful, and realistic, and being related to errors lower than 9.1 × 10⁻⁹. Therefore, these results can be considered as global solutions of the optimization process. Moreover, based on the lower errors obtained from the optimization process, it was possible to affirm that the one-diode model is suitable to model the I-V curve of perovskite solar cells. Finally, the estimated parameters suggested that the average ideality factor is close to 2 when the fill factor of the I-V curves is higher than 0.5. Lower fill factors corresponded to ideality that was higher than 3, linked to lower efficiencies, and high loses effects reflected on lower shunt resistances. Lower ideality factor of 1.4 corresponds to the best performing solar cells.

Keywords: perovskite solar cells; I-V curve; one-diode model; numerical sensitivity analysis

1. Introduction

The electrical performance of solar cells and panels is described by the I-V curve. This curve presents all the possible operative points, including the Short-Circuit Current (0, I_sc), Open Circuit Voltage (V_oc, 0) and the Maximum Power Point (V_mpp, I_mpp). Several numerical models have been developed to reproduce this curve at different conditions and illumination levels. Some of them are based on electrical circuits [1,2], partial differential equations or semiconductor equations [3,4], artificial intelligent technics [5,6], curve fitting [7,8], among others.

Circuital models based on the Kirchhoff’s current law, such as the one-diode model have been widely used to reproduce the I-V curve of different solar technologies [9,10] under different environmental conditions [11,12]. The one-diode model is characterized to be implicit, nonlinear, and multivariable. Therefore, there is no way to calculate an exact solution from the I-V data. Hence, up to 34 methods were proposed in literature to extract or estimate the five parameters related to the
model [2,13,14]. Where the shunt resistance \((R_{sh})\) is related to the leakage current across the surfaces involving pin-holes, grain boundaries, and charge recombination processes [15]. The series resistance \((R_s)\) is reflected in the voltage drops and is related to the conductivity of the layers and interphases, this parameter is affected by space charges, traps, or other barriers [16]. Virtually, a proportional relationship between the photo-generated current \((I_{ph})\) and irradiance intensity is observed. The diode saturation current \((I_o)\) is related to the material properties, junction configuration, recombination processes, and temperature. Finally, the ideality factor \((n)\) is related to the Shockley theory involving conduction, interfacial layers, transport, and recombination processes in the bulk and surface regions, which directly affects the shunt resistance and the open-circuit voltage [17,18].

However, since the parameters estimation of this model depend on different physical aspects (such as temperature, light condition, number of series cells, among others), mathematical assumptions to simplify or transform the problem, and the numerical method, which can be initial value dependent [13] or instable in the results [19], it is possible to obtain relatively large error in the optimization process [6], unrealistic parameters, such as negative resistances [20] or high diode ideality factors [21]. In the same way, instability in the estimated parameters has been observed under measurement uncertainty when data noise or fewer points of the \(I-V\) curve are considered [22]. These facts remark the complexity that is involved to estimate reliable parameters from the \(I-V\) curve.

In spite of the last drawbacks, the optimized parameters that are related to the circuit model have allowed for predicting the electrical performance of panels [11,23] and solar cells [24], reflect the dynamic of panels under different environment conditions [12], explain the transport and recombination process in solar cells [18,25], determine the minority carrier lifetime [26], investigate the interface state density quality [27] and losses effects [28], study the degradation effects [29], among others.

The ideality factor is the most reported parameter for different solar cells technologies. In the case of silicon solar cells, this value is between 1 and 2. \(n\) close to 1 indicates ideal junctions, while \(n\) equal to 2 would be related to degradation of the solar cell, non-uniformities on recombination centers, and shunt resistance effects [30]. In dye-sensitized solar cells, this factor is between 2 and 3 [31] and in organic solar cells this factor is higher than 2 [32]. In the case of Perovskite solar cells (PSC), ideality factors that are close to 2 have been reported due to carrier recombination and trap-assisted recombination under dark condition [33,34]. When several hole transport layer thicknesses are considered at dark conditions, the ideality factor has been found to range between 1.3 and 2.5 [35]. Additionally, based on the intensity dependence of \(V_{oc}\) under illumination conditions, an ideality factor between 1.7 and 1.9 has also been reported [36], and based on different device architectures, this parameter has been close to 1.0 for devices without hole transport layer (HTL) or even higher than 2 when considering the HTL [25]. However, due to the estimation of this parameter could be affected by different aspects such as hysteresis, slow relaxation processes, open-circuit voltage dependence of light intensity and temperature, capacitive effects and parasitic resistances, among others, the perovskite ideality factor from the dark \(I-V\) curve could produce values higher than 2 [37]. Therefore, another diode was included in the circuit model to agree with theoretical expectation [7], or methods that are based on light-intensity dependence, such as electroluminescence, \(V_{oc}\) as function of illumination intensity, or based on AC resistances, as electrochemical impedance spectroscopy was proposed to estimate this parameter [25,37].

In order to fully determine the parameters that are related to the one-diode model that represents p-i-n perovskite solar cells, 11 cells of approximately 1 cm\(^2\) of area were fabricated and characterized at standard test conditions. The \(I-V\) curve of these cells was fitted to the one-diode model to estimate the five parameters using a Genetic Algorithm combined with the Nelder-Mead method to minimize the mean square error between experimental data and the model results. Finally, a numerical analysis of the mean square error between the data and the model was carried out to determine feasible, realistic, and reliable values that represent the electrical behavior of perovskite cells. Hence, it was demonstrated that under a rigorous methodology and a numerical optimization process, the one-diode model is suitable to model the \(I-V\) curve of perovskite solar cells.
2. Materials and Methods

2.1. Perovskite Solar Cells

Taking into account that the reproducibility [38] and large area devices [39,40] play a crucial role in the photovoltaic performance of perovskite solar, different p-i-n planar devices (ITO/NiO2/CH3NH3PbI3/PC60BM/Rhodamine/silver) were fabricated with an active area between 1 and 1.5 cm² while using a previously reported protocol [41]. Briefly, devices were fabricated on Indium Tin Oxide (ITO) coated glass (Naranjo). The substrates were washed with neutral soap (Immunodet neutro) and sequentially sonicated in Deionized (DI) water, acetone, and isopropanol for 5 min. Then, ultraviolet ozone (UVO) treatment was done for 5 min at 100 °C. The NiO2 hole transporting material spin coated at 3000 rpm for 30 s with a 3 s ramp. To obtain a 430 ± 10 nm perovskite layer, a precursor solution of methylammonium iodide (Dyesol, Queanbeyan, Australia) and lead iodide (Alfa Aesar, Haverhill, MA, USA; 1:1 molar ratio; 55 wt %) in N,N-dimethylformamide (DMF) was deposited by spin-coating at 4000 rpm for 25 s. During spinning, 500 µL of Diethyleter (Aldrich, St. Louis, MO, USA) were dripped on the substrate after 10 seconds and the films were annealed at 65 °C for 1 min and 100 °C for 10 min. PCBM (1-Material) was deposited via spin-coating a 20 mg/mL solution in chlorobenzene (CB) at 2000 rpm for 30 s. Rhodamine 101 was deposited on top of the PCBM layer by spin coating a 0.5 mg/L solution at 4000 rpm for 30 s. Finally, to complete the devices, 100 nm thick silver electrodes were thermally evaporated under vacuum (≈10⁻⁶ mbar) at a deposition rate around ≈0.1 nm/s. The electrical performance of these devices was measured without mask at standard test conditions using a 4200SCS Keithley system (Tektronix, Beaverton, OR, USA) and an Oriel sol3A sun simulator (Newport Corporation, Irvine, CA, USA). From different batches fabricated, 11 cells that represent different electrical performances were intentionally selected. These cells showed different I-V curve characteristics, as shown in Figure 1 and Table 1.

![Figure 1. I-V curve of perovskite solar cells.](image)

**Table 1.** Electrical performance of perovskite solar cells.

| Cell | Area (cm²) | Efficiency (%) | Fill Factors (FF) | Voc (V) | J (mA/cm²) |
|------|------------|----------------|-------------------|--------|------------|
| 1    | 1.000      | 4.674          | 0.674             | 0.878  | 7.889      |
| 2    | 1.000      | 4.683          | 0.328             | 0.776  | 18.376     |
| 3    | 1.000      | 4.622          | 0.344             | 0.789  | 17.044     |
| 4    | 1.000      | 5.024          | 0.331             | 0.850  | 17.858     |
| 5    | 1.200      | 10.684         | 0.598             | 0.947  | 18.866     |
| 6    | 1.500      | 9.813          | 0.638             | 0.992  | 15.508     |
| 7    | 1.350      | 10.458         | 0.652             | 1.021  | 15.722     |
| 8    | 1.000      | 12.188         | 0.671             | 1.010  | 17.978     |
| 9    | 1.000      | 10.948         | 0.668             | 1.011  | 16.215     |
| 10   | 1.000      | 9.349          | 0.592             | 0.968  | 16.306     |
| 11   | 1.000      | 9.408          | 0.642             | 0.990  | 14.811     |
2.2. Numerical Methods Used to Extract the One-Diode Parameters

The one-diode model is characterized to be implicit, nonlinear, and multivariable (Equation (1)). This model showed the relationship between the current \( I \) and voltage \( V \) of solar device, the five parameters (photo-generated current, diode saturation current, ideality factor, shunt, and series resistances) and thermal voltage \( V_T \) that depends on the temperature, the Boltzmann constant \( k \), and electron charge \( q \), Equation (2).

\[
I = I_{ph} - I_0 \left( e^{\frac{V + I R_s}{R_sh}} - 1 \right) - \frac{V + I R_s}{R_sh} \tag{1}
\]

\[
V_T = k T / q \tag{2}
\]

Different numerical methods have been proposed in literature to estimate the five parameters that are related to one-diode model from the \( I-V \) curve data. Some of them are called exact because these parameters are expressed explicitly from algebraic manipulation. To obtain analytical expression for these parameters, most exact methods evaluate one-diode model equation and his derivative at specific points of the \( I-V \) curve, such as \((V_{oc}, 0), (0, I_{sc}), \) and \((V_{mpp}, I_{mpp})\). Moreover, to extract the parameters, some assumptions have been incorporated to simplify the iterative process or reduce the number of variables to be estimated. In Tables 1 and 2 were summarized and correlated the assumptions and implications to some common exact methods reported in literature [17,42–46]. Corresponding the most part of these assumptions to the resistances that are involved in the model. For instance, if \( R_s \) is approached to zero, then the exponential term of the Equation (1) can be simplified to \( e^{\frac{V}{R_s}} \) (assumption 1). If \( R_{sh} \) is approached to infinity, then the term \( \frac{V + I R_s}{R_{sh}} \) can be neglected (assumptions 2–4). If Equation (1) is evaluated at the short circuit current point, then the diode current can be simplified (assumptions 5–7). If Equation (1) is evaluated at the maximum power point (assumption 8), then the term “\(-1\)” can be neglected [45]. Moreover, if high illumination conditions are considered, then assumptions 9 and 10 can be applied [17]. Finally, if \( I_{ph} \) is approached to \( I_{sc} \) (value that is known), then just four variables can be estimated (assumption 11).

| No. | Assumptions | Implications |
|-----|-------------|--------------|
| 1   | \( e^{\frac{V}{R_s}} \gg e^{\frac{I R_s}{R_{sh}}} \) | Neglect \( e^{\frac{I R_s}{R_{sh}}} \) |
| 2   | \( I = \frac{I_0}{V} e^{\frac{I R_s}{R_{sh}}} \gg \frac{I_0}{R_{sh}} \) | Neglect \( \frac{I_0}{R_{sh}} \) |
| 3   | \( \frac{I_0}{R_{sh}} \ll \frac{1}{R_{sh}} \) | \( R_{sh} \approx R_{sh} - R_s \) |
| 4   | \( R_s \ll R_{sh} \) | \( R_{sh} \approx 0 \) and \( R_s + R_{sh} \approx R_{sh} \) |
| 5   | \( I_{ph} + I_0 \ll I_0 e^{\frac{I R_s}{R_{sh}}} \ll \frac{I_0}{R_{sh}} \) | \( I_{ph} + I_0 = I_{sc} \) |
| 6   | \( I_0 \left( e^{\frac{I R_s}{R_{sh}}} - 1 \right) \ll I_{ph} - \frac{(I_0 R_s)}{R_{sh}} \) | Neglect \( I_0 \left( e^{\frac{I R_s}{R_{sh}}} - 1 \right) \) |
| 7   | \( e^{\frac{(V_{mpp} + I_{mpp} R_s)}{R_{sh}}} \ll 1 \) | \( I = I_{ph} - I_0 \left( e^{\frac{I R_s}{R_{sh}}} - 1 \right) - \frac{V + I R_s}{R_{sh}} \approx I_0 \) |
| 8   | \( \frac{V_{mpp}}{R_{sh}} \ll I_{sc} \) | Neglect \( \frac{V_{mpp}}{R_{sh}} \) |
| 9   | \( \frac{V_{mpp}}{R_{sh}} \ll I_{sc} \) | Neglect \( \frac{V_{mpp}}{R_{sh}} \) |
| 10  | \( I_{ph} \gg I_0 \left( e^{\frac{I R_s}{R_{sh}}} - 1 \right) + \frac{(I_0 R_s)}{R_{sh}} \) | \( I_{ph} \approx I_{sc} \) |

Six exact methods that are commonly suggested in literature that involved the last assumptions are shown in Table 3. Due to that this kind of methods were developed to obtain quickly results and...
the number of assumptions are linked to the model simplicity, the generality, and accuracy of the solution can be compromised.

Table 3. Common exact methods and their assumptions (Assumptions numbered according to Table 2).

| References | Assumptions |
|------------|-------------|
| [42]       | X X X X X  |
| [43]       | X X X     |
| [44]       | X X       |
| [17]       | X X X     |
| [45,46]    | X X X X   |

Other methods are called numerical because they evaluate the one-diode equation and its derivative in different points of the $I-V$ curve, obtaining a set of nonlinear equations that can be solved using Newton-Raphson method [6,29], iterative process [47], among others. Additionally, when the numerical methods used to estimate the parameters required to calculate numerically the slope at $V_{oc}$ and/or the slope at $I_{sc}$ as initial conditions, instability and non-convergence of the solution can appear. Moreover, some of these methods can be sensitive to initial conditions [19].

To figure out these problems, numerical methods that are related to artificial intelligence, such as particular swarm [11], Genetic Algorithm (GA) has been successfully used to extract the five parameters of the one-diode model [5,48]. In these cases, one common way to express the parameter estimation as an optimization problem is minimizing the mean square error (Equation (3)) between the current measured ($i_{exp}$) and the current calculated evaluating the Equation (1) as a function of the five parameters. Where the samples corresponded to the number of points that are considered in the $I-V$ curve.

$$MSE = \frac{1}{\text{samples}} \sum_{k=1}^{\text{samples}} \left( i_{exp}(k) - i(I_{ph}, I_o, n, R_{shunt}, R_{series}, k) \right)^2$$  \hspace{1cm} (3)

3. Results

With the aim of obtaining the five parameters according to the one-diode model for a broad range of performance PSCs, the $I-V$ curves of devices fabricated and characterized in Section 2 (see Figure 1 and Table 1) were fitted to the circuit model. This process was divided in two parts. As an example, in the first part, the analysis was performed to Cell 1, which is a device with lower efficiency and short circuit current (see Table 1). For that, different numerical methods were used to extract the five parameters (see Tables 2 and 3). In the second part, the analyses were extended to other cells using the method that shows the best fitting performance. Note that in order to have a good validation of our method, the efficiencies of the studied devices ranged between 4.6 and 12.19%, Fill Factors (FF) between 0.3 and 0.7, open circuit voltages between 0.7 and 1 V, and short circuit current densities ($J$) between 7 and 18 mA/cm$^2$. The variability of these main variables indicated a broad range of electrical performance to be analyzed.

3.1. Extracting Parameters Using Different Exact and Numerical Methods

The electrical performance of cell 1 represented by the $I-V$ was fitted to the one-diode model using the six exact methods described on Table 3. Additionally, due to Genetic Algorithm (GA) explores global solutions and the method does not required any assumptions, constrains or derivatives, it is suitable to the paradigm addressed here (Equation (3)), in which the equation to fit is non-linear and multivariable [49].

The GA was defined by a mutation rate of 0.95 with 100 individuals in the population and 40 generations, tournament selection, and rank algorithm is considered [50]. The chromosome is
determined by the five parameters of interest and the fitness function by the mean square error (MSE) between the current measured ($I_{exp}$) and the one-diode model evaluated at each point of the $I$-$V$ curve, Equation (3).

The five parameters estimated and the MSE between the data and the fitting process are shown in Table 4. Notice that, in all cases, the errors were lower than $10^{-4}$, values that are in the same order as those commonly published in literature by implicit and explicit methods [11]. In the case of GA, the error was in the same order of evolutionary algorithms when synthetic data were used [49], indicating a good fitting and reproducibility of the $I$-$V$ curve.

**Table 4.** One-Diode parameters for cell 1.

| Method | Error      | $I_{ph}$ (mA/cm$^2$) | $I_o$ (µA/cm$^2$) | $n$ | $R_s$ (Ω·cm$^2$) | $R_{sh}$ (Ω·cm$^2$) |
|--------|------------|----------------------|-------------------|-----|------------------|---------------------|
| [42]   | $2.329 \times 10^{-4}$ | 7.865                | 23.127            | 6.262 | $-13.138$        | 3623.148            |
| [43]   | $2.326 \times 10^{-4}$ | 7.848                | 17.834            | 5.997 | $-10.588$        | 3633.737            |
| [44,51]| $3.681 \times 10^{-9}$ | 7.902                | 0.0288            | 2.743 | 5.980            | 3617.168            |
| [17]   | $2.152 \times 10^{-4}$ | 7.837                | 0.041             | 6.935 | $-14.638$        | 3623.148            |
| [45]   | $3.056 \times 10^{-4}$ | 7.872                | 3.471             | 4.720 | $-7.912$         | 3631.061            |
| [46]   | $4.262 \times 10^{-6}$ | 7.893                | 1.681             | 4.312 | 1.855            | 3621.293            |
| GA     | $4.803 \times 10^{-10}$ | 7.899                | 0.023             | 2.697 | 6.443            | 3392.119            |

The GA method that explores global solution showed the lowest error, followed by the oblique asymptote method proposed by Toledo et al. [51] that considers just two assumptions (Table 3). However, the method proposed by Khan et al. [17], which considers the largest number of assumptions obtained higher error, higher ideality factor, and negative series resistance, which lack physical meaning. These results confirmed that methods with less assumptions give more realistic parameters. Moreover, high ideality factors are correlated to negatives series resistances. Aspects mentioned in literature [13].

Due that $I_{ph}$ did not show significant changes (Table 4), a numerical sensibility analysis of error when considering the other four parameters was carried out with the aim to define feasible values. The MSE behavior as function of the estimated parameters is showed in Figures 2 and 3 while considering the logarithm of the MSE to improve visualization.

![Figure 2](image-url)  
**Figure 2.** Mean Squared Error (MSE) behavior as function of ideality factor and diode saturation current for Cell 1. Bar on the right denotes the MSE logarithm.
A small decrease on parameters from the sensitivity analyses for all cells are shown in Table 5. Notice that the MSE is lower to perform better. Being the local minimums the most common issues in optimization problems. For that reason, the solution is a trade of between the five parameters, the realistic and reliable parameter values that describe the electrical performance of this cell and minimize the MSE correspond to the parameters shown in Table 4 by GA, this set of parameters can be considered as a global solution.

3.2. One-Diode Model Parameters for Perovskite Solar Cells

In the case of the resistances that are involved in the model, different local regions with lower errors are obtained, even with negative values, see Figure 3. In these cases, negative or unrealistic resistances, trends to increase the ideality factor and the saturation current to minimize the MSE. Similar behavior was shown by some exact methods (Table 4). Variation of Shunt resistance did not show significant changes on MSE (Figure 3b). These graphical results suggested that this optimization problem is characterized by many feasible local minimums. However, due to the presence of multiple local minimums, the solution is a trade of between the five parameters, the realistic and reliable parameter values that describe the electrical performance of this cell and minimize the MSE correspond to the parameters shown in Table 4 by GA, this set of parameters can be considered as a global solution.

These results illustrate that the problem of estimate these five parameters from the I-V curve is very sensitive to small differences in the parameters that are involved in the one-diode model equation. In the case of $I_0$ and $n$ (Figure 2), a small increase on the ideality factor causes a great decrease on the exponential function value, which can be compensated by increasing the $I_0$ value and vice-versa. A small decrease on $n$ can be compensated by decreasing the $I_0$ value or changing the series resistances by negative values (Figure 3a), behavior showed in Table 4. However, the Figure 2 suggested that the ideality factor has to be higher than 2.00 in order to minimize the MSE.

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These graphical results suggested that this optimization problem is characterized by many feasible local minimums. However, due to the presence of multiple local minimums, the solution is a trade of between the five parameters, the realistic and reliable parameter values that describe the electrical performance of this cell and minimize the MSE correspond to the parameters shown in Table 4 by GA, this set of parameters can be considered as a global solution.

3.2. One-Diode Model Parameters for Perovskite Solar Cells

From the last results, it is easy to see why numerical methods that search for local solutions could be trapped in a specific region, and why methods, such as GA, which explore global solutions could perform better. Being the local minimums the most common issues in optimization problems. For that reason, the next analyses were carried out while using the GA method combined with the Nelder-Mead method to explore global solutions, refining the search, and minimizing the MSE [52]. Additionally, based on the relationship between the parameters involved in the one-diode equation that represents the electrical behavior showed by the I-V curve, a sensitive analysis is performed by changing the diode saturation current, ideality factor, and resistances obtained from the optimization process.

Figures 4–6 showed representative cases of the sensitivity analysis of MSE. For each case, the feasible range for the ideality factor that minimize the MSE is shown. The complete set of parameters from the sensitivity analyses for all cells are shown in Table 5. Notice that the MSE is lower than $9 \times 10^{-9}$ in all cases, indicating a successful fitting, as it was mentioned before.

![Figure 3. Mean Squared Error (MSE) behavior as function of ideality factor and series (a) and shunt (b) resistances for Cell 1. Bar on the right denotes MSE logarithm.](image-url)
Energies are characterized by average series resistance of 9.78 Ω and efficiency. Devices with a Fill Factor higher than 0.5. Other cases related to the expected range that are discussed in literature (between 1.7 and 2) correspond to lower efficiencies. Devices with a Fill Factor higher than 2.9 corresponded to lower efficiencies.

As it can be seen in Table 5, the lower ideality factor corresponds to the device with higher efficiency. Devices with $n$ in the expected range that are discussed in literature (between 1.7 and 2) are characterized by average series resistance of 9.78 Ω, average shunt resistances of 1672 Ω and Fill Factor higher than 0.5. Other cases related to the expected range that are discussed in literature (between 1.7 and 2) correspond to lower efficiencies.

Figure 4. Mean Squared Error (MSE) behavior as function of the estimated parameters for cell 5. MSE as function of ideality factor and diode saturation current (a), and MSE as a function of the ideality factor and series resistance (b).

Figure 5. Mean Squared Error (MSE) behavior as function of the estimated parameters for cell 8. MSE as function of ideality factor and diode saturation current (a), and MSE as function of the ideality factor and series resistance (b).

Figure 6. Mean Squared Error (MSE) behavior as function of the estimated parameters for cell 10. MSE as function of ideality factor and diode saturation current (a), and MSE as function of the ideality factor and series resistance (b).

As it can be seen in Table 5, the lower ideality factor corresponds to the device with higher efficiency. Devices with $n$ in the expected range that are discussed in literature (between 1.7 and 2) are characterized by average series resistance of 9.78 Ω, average shunt resistances of 1672 Ω and Fill Factor higher than 0.5. Other cases related to the expected range that are discussed in literature (between 1.7 and 2) correspond to lower efficiencies.
Factor higher than 0.5. Other cases related to $n$ higher than 2.9 corresponded to lower efficiencies and FFs. This result is congruent with a defective cell or high loses effect due that variables, such as $R_{sh}$, $I_o$, and $n$ are reflected in the recombination processes.

Table 5. One-diode parameters for Perovskite solar cells.

| Cell | Error | $I_{ph}$ (mA/cm$^2$) | $I_o$ (nA) | $n$ | $R_s$ (Ω·cm$^2$) | $R_{sh}$ (Ω·cm$^2$) |
|------|-------|----------------------|------------|----|------------------|------------------|
| 1    |       | 7.899                | 0.023      | 2.697 | 6.443            | 3392.119         |
| 2    |       | 17.160               | 3088.873   | 4.100 | 0.200            | 67.629           |
| 3    |       | 17.933               | 1401.235   | 4.057 | 0.200            | 64.984           |
| 4    |       | 0.019                | 0.331      | 2.074 | 9.648            | 586.058          |
| 5    |       | 15.662               | 0.238      | 2.151 | 9.981            | 1195.976         |
| 6    |       | 15.852               | 0.240      | 2.216 | 9.661            | 1491.744         |
| 7    |       | 18.051               | 5.993 × 10$^{-5}$ | 1.486 | 9.747            | 3184.295         |
| 8    |       | 16.263               | 3.976 × 10$^{-3}$ | 1.780 | 9.979            | 3951.715         |
| 9    |       | 16.581               | 39.718     | 2.949 | 5.514            | 352.362          |
| 10   |       | 15.061               | 0.002      | 1.705 | 11.318           | 828.667          |

4. Discussion

In order to determine feasible and reliable one-diode parameters that represent the electrical performance of PSC, five common exact methods that are proposed in literature were used to estimate the parameters based on the $I-V$ curve. From these results, it was showed that sometimes, these exact methods could obtain parameter estimations with low fitting error but lacking physical meaning due to negative resistances and higher ideality factors, as it has been reported in literature [13]. However, by combining the GA with Nelder-Mead method, it was possible to explore global solutions and minimize the error between the data and model, being these errors lower than those published in the literature [2,13]. Becoming this procedure in a powerful tool to fully estimate the parameters that are related to one-diode model, avoiding issues, such as initial condition and physical or mathematical assumptions to simplify the optimization process.

Based on the MSE behavior showed graphically through maps as a function of the estimated parameters, it was possible to determine feasible and reliable solutions to the circuit model. Showing that the problem of estimate the one-diode model parameters from the $I-V$ curve is very sensitive to small differences in the parameters that are involved, and that different parameter combinations lead to the reduction of the MSE even by solutions lacking physical meaning as negative resistances, being these results local minimal solutions defined by feasible, but not realistic, regions. However, MSE lower than 1 × 10$^{-9}$ could be considered as a good metric to evaluate the performance fitting and determine the more meaningful and reliable parameter estimation. These solutions could be considered as a global minimum.

When considering the five parameters estimated for each perovskite solar cell at standard test condition. These results suggested that the ideality factor is in average close to 2 when the FF is higher than 0.5. In this sense, the ideality factor that was obtained for perovskite agreed with values published in literature using other measures, such as electroluminescence [25] or electrochemical impedances spectroscopy [37]. Lower FF are linked to ideality factor higher than 3 and low series resistances, fact that could be correlated to defects such as pinholes, which is reflected on the low shunt resistances, indicating high losses effects. An ideality factor of 1.4 was obtained for the best performing cell.

5. Conclusions

In this paper p-i-n perovskite solar cell with an active area of approximately 1 cm$^2$ were fabricated and characterized. To estimate feasible and reliable parameters that are related to the one-diode model and represent the electrical performance of p-i-n PSC, two powerful numerical methods, called
Nelder-Mead method and Genetic algorithm, were mixed. This procedure searches for global solution and no assumptions were required, ensuring errors lower than $1 \times 10^{-9}$ in all cases.

The dependence of the error (MSE) to the one-diode model parameters were shown for first time graphically through maps with the aim to illustrate why different common numerical methods obtained lower errors and solutions lacking physical meaning as negative resistances. Based on this error behavior and considering that the fitted errors were lower than $1 \times 10^{-9}$, the estimated parameters that represented the electrical performance of devices can be considered as a global minimum of the optimization problem.

This procedure is reliable to estimate not only the ideality factor, which is related to the quality of the cells, but the series and shunt resistances and the saturation current. Therefore, due to the $I$-$V$ curve data of devices (that define their electrical performance in all operative points) at standard test conditions were considered, the estimated parameters represent these conditions, and for that, no extra measures, such as changing the light intensity, electroluminescence, or dark measures are necessary. From this way, we can estimate parameters related to electrical performance based on common data, such as described on solar devices datasheet.

Finally, based on the lower MSE obtained from the fitting process, it was possible to affirm that the one-diode model is suitable to model the $I$-$V$ curve of perovskite solar cell technology, even for low performance devices characterized by low fill factor.

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