Doppler Frequency Estimation for a Maneuvering Target Being Tracked by Passive Radar Using Particle Filter

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Abstract—In this paper, we estimate Doppler frequency of a maneuvering target being tracked by passive radar using two types of particle filter, the first is “Maximum Likelihood Particle Filter” (MLPF) and the second is “Minimum Variance Particle Filter” (MVPF). By simulating the passive radar system that has the bistatic geometry “Digital Video Broadcasting-Terrestrial (DVB-T) transmitter / receiver” with these two types, we can estimate the Doppler frequency of the maneuvering target and compare the simulation results for deciding which type gives better performance.

Index terms—Passive Radar, Doppler Frequency, Maneuvering Target, Maximum Likelihood Particle Filter, Minimum Variance Particle Filter.

I. INTRODUCTION

PASSIVE radar is a bistatic radar that detects and tracks targets by processing reflections from non-cooperative sources of illumination. It has many advantages, such as resistant to jammers and does not need a dedicated frequency band. This radar is equipped with two antennas: The first antenna is the direct antenna that receives the direct signal, and the second antenna is the surveillance antenna that receives targets’ echoes and multipath signals [1], [2]. The direct signal is reconstructed to detect targets’ echoes [3]-[5]. Many researches have been conducted studying this radar, such as studying and analyzing of signals of non-cooperative transmitters (e.g., Frequency Modulation (FM) radio, Global System for Mobile communication (GSM), Digital Video Broadcasting-Terrestrial (DVB-T), and Digital Audio Broadcasting (DAB)) [1], [2], [6]-[9], studying of the interference of the direct signal on the surveillance channel [10], [11], detection of “maneuvering/non-maneuvering” targets [12]-[14], and estimation of their parameters (e.g., Doppler frequency, velocity, acceleration, and coordinates) [2], [15]-[19].

Doppler frequency of a non-maneuvering target is estimated by applying the Maximum Likelihood method to the output of a bank of matched filters, which are tuned to different Doppler frequencies [1], [17]. But in the case of a maneuvering target, this way is ineffective because the velocity and direction of this target change non-linearly during small periods. Therefore, non-linear tracking filters should be used, such as Extended Kalman Filter (EKF), Unscented Kalman Filter (UKF) [20]-[22], and Particle Filter (PF) [22]-[31]. Many researches have indicated that the (PF) has better performance for estimating parameters that change non-linearly at low SNR, because it depends on the Monte Carlo method, [2], [22]-[24]. According to the processing method, the (PF) has the following two types: MLPF and MVPF [23], [24]. In this paper, we estimate the Doppler frequency of a maneuvering target by simulating these two types within a passive radar system that has the bistatic geometry “DVB-T transmitter/receiver”. Then we suggest the optimal application for each type by comparing and analyzing the simulation results.

The paper is organized as follows. Section II introduces the passive radar system with a maneuvering target. Section III illustrates the particle filter with its two types (MLPF and MVPF), which will be used for estimating the Doppler frequency for the maneuvering target. Section IV shows simulating the passive radar system with these two types and concentrates on discussing the simulation results. Section V concludes the paper.

II. PASSIVE RADAR SYSTEM

It has the following bistatic geometry: one DVB-T transmitter and one receiver with two receiving antennas, taking into consideration that there is one maneuvering target, as shown in Fig. 1 where $T_x$ is the non-cooperative transmitter, $R_1$ is the receiver, $T_m$ is the maneuvering target, $R_2$ is the range between the transmitter ($T_x$) and the target ($T_m$), $R_1$ is the
effective range, \((x_a, y_a, z_a)\) are the Cartesian coordinates of the observed target \((T_a)\), D is the distance from the transmitter \((T_a)\) to the receiver \((R_x)\), SC refers to “Surveillance Channel”, and DC refers to “Direct Channel”.

After suppressing the interference in the surveillance channel and mitigating multipath signals based on the properties of the DVB-T signal that uses the Orthogonal Frequency Division Multiplexing (OFDM) modulation technique, the echo signal of the observed target is given in (1), [2], [23], [25].

\[
Y(t) = A(t) e^{j \varnothing(t)} S(t - \tau) + n(t); \quad t = 0: T_p
\] (1)

where \(t\) is the discrete time of the observation, \(Y\) is the observation signal, \(A\) is the amplitude, \(\varnothing\) is the phase, \(S\) is the delayed direct signal with the time delay \((\tau)\), \(n\) is the Additive White Gaussian Noise, and \(T_p\) is the duration of the processed data window.

For estimating the Doppler frequency of the maneuvering target by the particle filter, we will briefly explain this filter and its two types, as presented in the following section.

### III. PARTICLE FILTER

It is a filtering method that depends on the Monte Carlo approximation and recursive Bayesian estimation. It mainly consists of propagating, in a non-linear way, weighted particles in a domain of a studied state. With helping of observations from a studied system, the weight and state of each particle are processed by a method for getting estimation results. For effective estimation, a resampling step should be applied for re-propagating the particles in a different domain for the studied state [26], [27]. This process is achieved by processing the output of the following two equations for each particle: The state equation and measurement equation, which are given in (2) and (3), respectively [26]-[28].

\[
x_t = f(x_{t-1}) + v_t
\] (2)

\[
Z_t = h(x_t)
\] (3)

where \((t, (t - 1))\) are the current and previous measurement time, respectively, \(x\) is the state vector \((x \in \mathbb{R}^n)\), \(f\) is a non-linear function and it is a known function, \(v\) is the state noise vector \((v \in \mathbb{R}^m)\); \(v \sim \mathcal{N}(0, \sigma_v^2)\), \(Z\) is the measurement signal \((Z \in \mathbb{R}^nx)\), and \(h\) is a non-linear function and it is a known function. The symbol \((\mathcal{N}(m, \sigma_z^2))\) denotes the Gaussian density function with the mean \((m)\) and variance \((\sigma_z^2)\).

In the passive radar system, the state vector is \((x = [A, \varnothing, f_0, T]^T)\), and the dynamics of its parameters are given in (4), [2], [23], [25].

\[
\begin{bmatrix}
A_t \\
\varnothing_t \\
\tau_t
\end{bmatrix} =
\begin{bmatrix}
A_{t-1} \\
\varnothing_{t-1} + 2\pi f_d t_{t-1} T_p \\
\tau_{t-1} - \frac{f_{d t_{t-1}} T_p}{f_0}
\end{bmatrix} +
\begin{bmatrix}
v^A_t \\
v^\varnothing_t \\
v^\tau_t
\end{bmatrix}
\] (4)

where \(f_d\) is the Doppler frequency, \((v^A, v^\varnothing, v^\tau)\) are the Gaussian noises, \(f_0\) is the carrier frequency, and \(T\) denotes the transposition.

The particle filter has two types according to its processing method, as presented in the following two subsections.

#### A. MLPF

It depends on moving the particles’ distribution toward the region of highest likelihood by using the (EKF) [29], [30]. It is achieved by implementing the following steps, taking into consideration that \((p)\) is the Probability Density Function [25], [26], [28], [31].

a) Initialization: Propagating particles with different states and equal weights. The initial weights are as follows: \((w_{i=0}^t = 1/N_s)\), where \(N_s\) is the number of particles and \(i\) is the index of these particles; \(i = 1: N_s\). See the red particles in Fig. 2.

b) Calculating the current weights of the particles at the time \((t)\) by the following equation, taking into consideration the green particles in Fig. 2.

\[
w_i^t = p(Y_t/x_i^t) = p(Y_t/h(x_i^t)) = w_{i(t-1)}^t \cdot \mathcal{N}(Y_t - h(x_i^t), R_t)
\] (5)

where \((w_{i(t-1)}^t, w_i^t)\) are the current and previous weight for the particle \((i)\), respectively, and \(R_t\) is the covariance matrix [25], [28], [31].

c) Normalizing the calculated weights by the following equation:

\[
w_i^t = \frac{w_i^t}{\sum_{i=1}^{N_s} w_i^t}
\] (6)

d) The studied state is estimated by the following equation:

\[
\hat{x}_t = \sum_{i=1}^{N_s} (w_i^t \cdot x_i^t)
\] (7)

### Fig. 1. Bistatic geometry of passive radar
e) Resampling: The particles that have high weights are selected for propagating new particles with different states and equal weights; \( \{w_t^i = (1/N_s); \ i = 1:N_s\} \). See the green and black particles in Fig. 2.

f) Re-implementing the steps (b \( \rightarrow \) e) at each observation time (\( t \)).

By focusing on Fig. 2 and Fig. 3, we notice that the variance between the resampled particles is equal in the case of MLPF and unequal in the case of MVPF. Therefore, MVPF has an additional advantage compared with MLPF, as presented later.

To illustrate the difference between MLPF and MVPF, we will suppose the following estimation with \( N_s = 28 \) (particles). We want to estimate the real Doppler frequency that equals (-781.8 (Hz)) by these two types, taking into consideration the proposed probability density for the weights of the processed particles, as shown in Fig. 4 and Fig. 5. By simulating the mentioned estimation, we notice that the resampled particles are distributed only around the real Doppler frequency (main event) in the case of MLPF, as shown in Fig. 4, whereas they are distributed around the main event and sudden event in the case of MVPF, as shown in Fig. 5. The sudden event cannot be observed in the case of MLPF, thus using (MVPF) will improve the performance of the passive radar for tracking targets in sudden environments.
IV. SIMULATION AND RESULTS

A. Simulation

MATLAB software is used for simulating the particle filter with the passive radar system that consists of the DVB-T transmitter, Additive White Gaussian Noise channel with one maneuvering target, and receiver, as shown in Fig. 1. For simplicity, we consider that the parameters of the state vector \((A, \phi, \tau)\) are determined at each measurement time. This simulation is achieved with the technical characteristics for the transmitter, receiver and target, as listed in Table I.

| TABLE I | TECHNICAL CHARACTERISTICS FOR TRANSMITTER, RECEIVER AND TARGET |
|---------|---------------------------------------------------------------|
| ERP     | 50 (KW)                                                     |
| Carrier frequency | 474 (MHz)                             | Duration of OFDM symbol | 1.1 (ms) |
| Bandwidth | 8 (MHz)                                               | Cartesian coordinates | (0, D, 0) |
| Transmission mode / modulation | 8K mode / 64QAM                    | D                        | 5 (Km) |
| Code Rate | 7/8                                                     | Losses \((L_e)\) | 1 (dB) |
| DVB-T Transmitter |                                                 |                           |    |
| Surveillance antenna gain \((G_{RSA})\) | 22 (dB) | Time difference between two consecutive observations | 85 (ms) |
| Gain of direct antenna | 2.5 (dB) | \(T_p\) | 2.2 (ms) |
| Cartesian coordinates | (0, 0, 0) | Losses \((L_r)\) | 1 (dB) |
| \(\sigma_{e_{RSA}}^2\) | 1.8² (Hz²) | Noise Figure \((F_e)\) | 2 (dB) |
| Target | Monostatic RCS | 6 (m²) | Initial coordinates | (9, 8, 3.5) (Km) |
| Receiver |                                               |                           |    |

We consider that the observed target moves according to the path shown in Fig. 6, and its velocity changes according to Fig. 7. Therefore, the signal-to-noise ratio (SNR) of the target’s echo signal changes according to Fig. 8, taking into consideration that the mentioned target is detected with a false alarm probability \((10^{-4})\). The indicated parameter (SNR) is given in (10), [2], [7].

\[
SNR = \frac{P_t G_t G_{RSA} A^2 \sigma_{RCS}}{(4\pi)^3 K T_0 B F_r L_t L_r R_1^2 R_2^2} \tag{10}
\]

where \(P_t\) is the transmitted power (watt), \(G_t\) is the transmitter antenna gain, \(\lambda\) is the transmitter wavelength (m), \(\sigma_{RCS}\) is the bistatic radar cross section (m²), \(K\) is Boltzmann’s constant, \(T_0\) is the effective noise temperature, and \(B\) is the receiver bandwidth (Hz).
B. Results and Notes

We performed the estimation of the Doppler frequency of the maneuvering target by MLPF and MVPF for the following two cases: \((N_s = 5)\) and \((N_s = 15)\). In the first case \((N_s = 5)\), the estimation accuracy was 2.4 (Hz) for MLPF and 4.3 (Hz) for MVPF, as shown in Fig. 9. In the second case \((N_s = 15)\), the resulting accuracy was 2.1 (Hz) for MLPF and 3.2 (Hz) for MVPF, as shown in Fig. 10.

Note: Estimation accuracy is related to the standard deviation of estimation errors, as given in (11), [29].

\[
\sigma_{ES} = \sqrt{\frac{1}{M-1} \sum_{i=1}^{M} (d_i - \mu)^2} \quad (11)
\]

where \(\sigma_{ES}\) is the Estimation Accuracy of a studied parameter, \(M\) is the number of observations, \(d\) is the estimation error that has the equation: \((d_i = true\ value_i - estimated\ value_i)\), and \(\mu\) is the mean of estimation errors.

By focusing on Fig. 9 and Fig. 10, we notice the following points: First, MLPF and MVPF have convergent performance in terms of estimation accuracy, and their performance is improved by increasing the number of particles. Second, MLPF has less complexity than MVPF because particles by MVPF are resampled based on calculating and analyzing the state probability of each particle, consequently the complexity of MVPF is increased by increasing the dimension of the state vector. Finally, these two types are suitable for tracking maneuvering targets, but the type (MVPF) has better performance for tracking these targets in the sudden environments, such as Decoy Flares or sudden crash of airplanes, because using this type leads to observe states that have low probabilities.

Note: The author of [2] had estimated the Doppler frequency of a maneuvering target by (MLPF) when he estimated target coordinates (at SNR=3dB) in the case of passive radar with multiple (DVB-T) transmitters and a receiver. The estimation accuracy in his case was approximately 2 (Hz), taking into consideration that the number of particles larger than our case. The lower value for the parameter (SNR) in [2] does not affect the comparison with the simulation results, because the particle filter can effectively estimate parameters that change very non-linearly at low SNR, [23], [24].

V. CONCLUSION

In this paper, the estimation of Doppler frequency of a maneuvering target has been performed by using the two types of particle filter: Maximum Likelihood Particle Filter and Minimum Variance Particle Filter. The characteristics of each type were checked by simulating a passive radar system that has the bistatic geometry (a DVB-T transmitter and a receiver). The simulation results have illustrated the efficiency of each type in terms of estimation accuracy, complexity, and a suitable application.

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