Measurement of the Cross Section for Prompt Diphoton Production in $p\bar{p}$ Collisions at $\sqrt{s} = 1.96$ TeV
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We report a measurement of the rate of prompt diphoton production in $p\bar{p}$ collisions at $\sqrt{s} = 1.96$ TeV using a data sample of 207 pb$^{-1}$ collected with the upgraded Collider Detector at Fermilab (CDF II). The background from non-prompt sources is determined using a statistical method based on differences in the electromagnetic showers. The cross section is measured as a function of the diphoton mass, the transverse momentum of the diphoton system, and the azimuthal angle between the two photons and is found to be consistent with perturbative QCD predictions.

PACS numbers: 13.83.Qk, 12.38.Qk

Diphoton ($\gamma\gamma$) final states are a signature of many interesting physics processes. For example, at the LHC, one of the main discovery channels for the Higgs search is the $\gamma\gamma$ final state. An excess of $\gamma\gamma$ production at high invariant mass could be a signature of large extra dimensions, and in many theories involving physics beyond the standard model, cascade decays of heavy new particles generate a $\gamma\gamma$ signature. However, the QCD production rate is large compared to most new physics, so an understanding of the QCD production mechanism is a prerequisite to searching reliably for new physics in this channel. In addition, the two-photon final state is interesting in its own right. Due to the excellent energy resolution of the CDF electromagnetic (EM) calorimeter, the 4-momenta of the two photons and is found to be consistent with perturbative QCD predictions.
example, a direct measurement of the transverse momentum of the $\gamma\gamma$ system ($q_T$), which is sensitive to initial state soft gluon radiation.

In perturbative Quantum Chromodynamics (pQCD), the leading contributions are from quark anti-quark annihilation ($q\bar{q} \rightarrow \gamma\gamma$) and gluon-gluon scattering ($gg \rightarrow \gamma\gamma$). The latter subprocess involves initial state gluons coupling to the final state photons through a quark box; thus, this subprocess is suppressed by a factor of $\alpha_s^2$ with respect to the $q\bar{q}$ subprocess. However, the rate is still appreciable in kinematic regions where the $gg$ parton luminosity is high, such as at low $\gamma\gamma$ mass. Because the probability for a hard parton to fragment to a photon is of order $\alpha_{em}/\alpha_s$, processes involving the production of one (zero) prompt photons and one (two) photons originating from parton fragmentation are also effectively of leading order (LO). Next-to-leading order (NLO) contributions include real and virtual corrections to the above subprocesses.

We have compared our experimental results to three predictions: DIPHOX [2], ResBos [3], and PYTHIA [4]. DIPHOX is a fixed-order QCD calculation that includes all of the above subprocesses at NLO (except for $gg \rightarrow \gamma\gamma$ which is present only at LO). Recently, NLO corrections for $gg \rightarrow \gamma\gamma$ have been calculated [5] and we have added these corrections to the DIPHOX prediction. The ResBos program includes subprocesses where the two photons are produced at the hard-scattering at NLO and fragmentation contributions at LO; but also resums the effects of initial state soft gluon radiation. This is particularly important for examination of the $\gamma\gamma q_T$ distribution, which is a delta function at LO and divergent as $q_T \rightarrow 0$ at NLO, and thus requires a soft gluon resummation in order to provide a physical description of the $\gamma\gamma$ data in this region. PYTHIA is a parton shower Monte Carlo program that contains the above processes at LO.

At hadron-hadron colliders, it is difficult to measure a fully inclusive $\gamma\gamma$ cross section due to the large backgrounds from quarks and gluons fragmenting into neutral mesons which carry most of the parent parton’s momentum. Isolation requirements are typically used to reduce these backgrounds. In this analysis, the isolation criterion requires that the transverse energy ($E_T$) sum in a cone of radius $R = 0.4$ in $\eta - \phi$ space [6] about the photon direction, minus the photon energy, be less than 1 GeV. This isolation requirement reduces the backgrounds from neutral mesons decaying into photons and photon production from fragmentation sources. The CDF isolation requirement effectively removes all contributions where both photons originate from fragmentation subprocesses. However, as will be noted later, some indication of single fragmentation subprocesses can still be observed in the CDF data.

The CDF II detector is a magnetic spectrometer which is described in detail elsewhere [10]. The central detector consists of a silicon micro-strip vertex detector inside a cylindrical drift chamber, both of which are immersed in the 1.4 T magnetic field of a superconducting solenoid. Outside the solenoid is the central calorimeter which is divided into an electromagnetic compartment (CEM) on the inside and hadronic compartment (CHA) on the outside. Both calorimeters are segmented into towers of granularity $\Delta \eta \times \Delta \phi \approx 0.1 \times 0.26$. The CEM consists of a scintillator-lead calorimeter along with an embedded multi-wire proportional chamber (CES) located near shower maximum at 6 radiation lengths. The CES allows for a position determination of the EM shower and for a measurement of the lateral shower profile. The average energy resolution of the CEM is $\sigma(E)/E = 13.5%/\sqrt{E \sin \theta}$ (with $E$ in GeV) and the position resolution of the CES is 2 mm for a 50 GeV photon. Another important component for this analysis is a preshower wire chamber (CPR) mounted between the magnet coil and the CEM, at about 1.2/$\sin \theta$ radiation lengths. The CPR detects photon candidates that have converted in the magnet coil and other material in the inner detector.

This analysis [11] uses events collected with a trigger that requires two photon candidates with $E_T$ greater than 12 GeV each. A requirement of $E_T$ greater than 14 GeV (13 GeV) for the leading (softer) photon candidate in the event is imposed in the offline analysis. The minimum transverse energy requirements for the two photon candidates are different in order to avoid the kinematic region where the NLO calculation is unstable due to the imperfect cancellation of the real and virtual gluon divergences.

In identifying photons, we impose fiducial requirements to avoid uninstrumented regions at the edges of the CES; as part of this criterion we require the pseudorapidity of the photon candidate to be in the interval $|\eta| < 0.9$. The reconstructed $z$-vertex for the collision is required to be less than 60 cm from the center of the detector. The ratio of the hadronic energy to EM energy (Had/EM) for the photon candidates must be less than 0.055+0.00045$\times E$, with $E$ the EM energy in GeV. The isolation energy is required to be below 1 GeV. Although only about 1% of showers from prompt photons have more than 1 GeV of additional energy in the isolation cone, about 15% of the photon showers fail the isolation requirement because of additional energy from the underlying event [12]. Photon candidates with any tracks ($p_T$ above 0.5 GeV) that can be extrapolated to them are rejected. The lateral profile of EM showers in the CES is compared to the profile of electrons measured in a test beam. The definition of the $\chi^2$ from the comparison can be found in Ref. [13]. We require the $\chi^2$ of the comparison to be less than 20 in the event selection and reject photon candidates with an additional CES cluster above 1 GeV [14]. The efficiencies for each event selection requirement, evaluated using a combination of PYTHIA Monte Carlo and data, are listed sequentially in Table [14].
The trigger efficiency per photon, measured using a single photon trigger, is approximately 80% at 13 GeV and rises to greater than 99% for photons above 15 GeV. The combined selection efficiency, including acceptance and trigger efficiency, is 15.2% per diphoton event.

After imposing all of the requirements, 889 two-photon candidates remain in our data sample. This sample includes background from neutral mesons such as π0 and η that decay to multiple photons. To estimate this background, we apply the statistical background subtraction method described in [17], which makes use of the differences on average between EM showers produced by single photons and by the multiple photons produced in neutral meson decays. The separation between single and multiple photon showers relies on the shower shape measured by the CES χ2 and the preshower conversion pulse height measured by the CPR. Since photons from the decay of neutral mesons with ET above 35 GeV are almost collinear in the lab frame, their shower shape in the CES is no longer distinguishable from a single-photon shower. To estimate the background contamination in this high ET region, the CPR has been utilized. The chance for a conversion to take place in the tracking volume or magnet coil (1.1 radiation lengths) and generating a hit in the CPR is higher for the multiple photons than for a single photon. We use the CES shower shape for photon showers with ET < 35 GeV and the CPR pulse height for ET > 35 GeV. For each photon candidate, we test whether the CES χ2 is less than 4 (low ET) or the photon candidate produces a pulse height in the CPR greater than one minimum ionizing particle (high ET). There are four possibilities for the final state: both candidates pass the test, the first candidate passes and the second fails, the first fails and the second passes, or both candidates fail (the first candidate has the higher ET). From the known efficiencies for photons and background to pass the χ2 and conversion tests, we can then determine the number of true γγ events (as well as the number of γγ-background, background-γ and background-background events). Using the two background techniques discussed, we determine that of the 889 candidates, 427 ± 59(stat) are real γγ events. From these events, the calculated acceptance and the integrated luminosity, we determine the diphoton cross sections for several kinematic variables.

The γγ mass distribution is shown in Fig. 1 along with predictions from DIPHOX, ResBos and PYTHIA. The qT distribution is shown in Fig. 2 and the Δφ distribution between the two photons is shown in Fig. 3. The vertical error bars on the data indicate the combined statistical and systematic uncertainties with the inner tick marks indicating the statistical uncertainty alone [19]. The PYTHIA predictions have been scaled (factor of 2) to the total measured cross section in all the figures. The cross sections as a function of these three different variables are also tabulated in Tables II, III and IV.

It should be noted that the background to the γγ signal has been determined independently for each kinematic bin as the background fraction can vary with the kinematics. Determining the background on a bin-by-bin basis increases the statistical uncertainty but decreases the systematic uncertainty.

The systematic effects include uncertainties on the selection efficiencies (11%), uncertainties from the background subtraction (20-30%) and from the luminosity determination (6%) [17].

We note some features of the theoretical predictions. The gg subprocess provides a significant contribution to diphoton production at low mass (~30 GeV/c2); the slight wiggle observed in the DIPHOX prediction is due to the very rapid falloff (with diphoton mass) of the gg subprocess compared to the qT subprocess. The Res-
Bos $q_T$ curve is smooth for the entire range, while the DIPHOX curve (as can be seen by the negative value in the first bin of Table III) is unstable at low $q_T$ due to the singularity noted earlier, and thus is not plotted in Fig. 2 for $q_T < 2$ GeV/c [15]. At the high $q_T$ end, DIPHOX displays a shoulder, a feature absent in the ResBos prediction. The ResBos curve lies above the DIPHOX one at $\Delta\phi$ values of the order of $\pi/2$ but also lies significantly below the DIPHOX curve at small $\Delta\phi$.

The observed differences between the predictions are expected. The fragmentation contribution in ResBos is effectively at LO. Since fragmentation to a photon is of order $\alpha_{em}/\alpha_s$, some 2→3 processes such as $gq \rightarrow gq\gamma$, where the quark in the final state fragments to a second photon, are of order $\alpha_{em}\alpha_s$ and are included in a full NLO calculation. These contributions are present in DIPHOX, but not in ResBos, which leads to an underestimate of the production rate in the latter at high $q_T$, low $\Delta\phi$, and low $\gamma\gamma$ mass. In particular, the shoulder at $q_T$ of approximately 30 GeV/c arises from an increase in phase space for both the direct and fragmentation subprocesses [15]. It is instructive to divide the DIPHOX predictions into two regions: $\Delta\phi > \pi/2$ and $\Delta\phi < \pi/2$.

We do so, and plot the $q_T$ prediction for the $\Delta\phi < \pi/2$ region in Fig. 2 in order to highlight this contribution. It is apparent that the bump in the DIPHOX prediction at a $q_T$ of approximately 30 GeV/c is due to the “turn-on” of the $\Delta\phi < \pi/2$ region of phase space. At $\Delta\phi$ values above $\pi/2$, the effects from soft gluon emission (included in ResBos but not in DIPHOX) are significant.

The data are in good agreement with the predictions for the mass distribution. At low to moderate $q_T$ and $\Delta\phi$ greater than $\pi/2$, where the effect of soft gluon emissions are important, the data agree better with ResBos than DIPHOX. By contrast, in the regions where the 2→3 fragmentation contribution becomes important, large $q_T$, $\Delta\phi$ less than $\pi/2$ and low diphoton mass, the data agree better with DIPHOX.

In this paper, we have presented results for $\gamma\gamma$ production in $p\bar{p}$ collisions at a center-of-mass energy of 1.96 TeV using a data sample twice that previously available. Good agreement has been observed with resummed and NLO predictions in different regions of phase space. For agreement in all areas, however, a resummed full NLO calculation will be necessary.

We thank the Fermilab staff and the technical staffs of the participating institutions for their vital contributions. This work was supported by the U.S. Department of Energy and National Science Foundation; the Italian Istituto Nazionale di Fisica Nucleare; the Ministry of Education, Culture, Sports, Science and Technology of Japan; the Natural Sciences and Engineering Research Council of Canada; the National Science Council of the Republic of China; the Swiss National Science Foundation; the A.P. Sloan Foundation; the Bundesministerium fuer Bildung und Forschung, Germany; the Korean Science and Engineering Foundation and the Korean Research Foundation.

| $\Delta\phi\gamma\gamma$ ($\pi$ rad) | CDF Data (pb/rad) | DIPHOX (pb/rad) | ResBos (pb/rad) | PYTHIA (pb/rad) |
|-----------------------------------|------------------|----------------|----------------|----------------|
| 0.0-0.2                           | 1.06 ± 0.52 ± 0.34 | 0.69           | 0.01           | 0.02           |
| 0.2-0.4                           | 0.89 ± 0.52 ± 0.32 | 0.56           | 0.23           | 0.09           |
| 0.4-0.6                           | 0.51 ± 0.63 ± 0.19 | 0.71           | 0.73           | 0.44           |
| 0.6-0.8                           | 3.34 ± 1.10 ± 1.04 | 1.83           | 3.08           | 1.09           |
| 0.8-1.0                           | 15.56 ± 2.59 ± 4.70 | 23.37         | 17.52          | 10.68          |

FIG. 1: The $\gamma\gamma$ mass distribution from the CDF Run II data, along with predictions from DIPHOX (solid), ResBos (dashed), and PYTHIA (dotted). The PYTHIA predictions have been scaled by a factor of 2. The inset shows, on a linear scale, the total $\gamma\gamma$ cross section in DIPHOX with (solid)/without (dashed) the $gg$ contribution.

FIG. 2: The $\gamma\gamma$ $q_T$ distribution from the CDF Run II data, along with predictions from DIPHOX (solid), ResBos (dashed), and PYTHIA (dotted). The PYTHIA predictions have been scaled by a factor of 2. Also shown, at larger $q_T$, are the DIPHOX prediction (dot-dashed) and the CDF Run II data (open squares : shifted to the right by 1 GeV for visibility) for the configuration where the two photons are required to have $\Delta\phi < \pi/2$. 

TABLE IV: A comparison of the cross section as a function of the $\gamma\gamma$ $\Delta\phi$ for the data and predictions from DIPHOX, ResBos and PYTHIA.
FIG. 3: The $\Delta \phi$ angle between the two photons from the CDF Run II data, along with predictions from DIPHOX (solid), ResBos (dashed), and PYTHIA (dotted). The PYTHIA predictions have been scaled by a factor of 2. The bump at $\Delta \phi = 0.3$ on the DIPHOX curve is unphysical; it is caused by the combination of collinear divergence and the anti-collinear cut [11].

We would like to thank C. Balazs, J. Ph. Guillet, E. Pilon, C. Schmidt and C.-P. Yuan for invaluable discussions.

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