Research of Focal Mechanism and Focal Depth of Qilian, Qinghai M₅.2 Earthquake

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Abstract. This paper selects the waveform records of 16 broadband digital seismic stations in the regional seismic network of Gansu province, Qinghai province, and Sichuan province involved inversion, use CAP focal mechanism solution method to calculate the Ms 5.2 earthquake which occurred in Qilian County, Qinghai Province, November 23, 2015. Obtained the focal mechanism solution of this earthquake is a strike-slip fault with thrust property. The inversion results show the optimal double couple solution is nodal plane I: The strike is 112°, the dip, 51.7°; and the rake, 24.5°. Nodal plane II: The strike is 7°, the dip, 71°; and the rake, 139°. Earthquake moment magnitude is Mₑ 5.2 and the optimal depth solution is 8km, which is consistent with the results of IGP-CEA. We calculate focal depth with the arrival time difference between sPn and Pn phases, the results is 6.6km, which agree with the CAP method results and verify the feasibility of this method.

1 Background

Focal depth is one of the most difficult parameters to accurately measure as a basic parameter of seismic space-time parameters. Accurate determination of focal depth is related to the correct understanding of a series of important issues such as focal process, fault structure, and stress field. For larger earthquakes, accurate determination of focal depth is an important reference factor for judging focal intensity. Because there are fewer seismic stations in the upper and lower directions, depth positioning is not as accurate as horizontal positioning and focal depth is a relatively difficult quantity to determine in earthquake location. The regional seismic network is usually based on a one-dimensional velocity model, using Pg (Sg) and Pn (Sn) phases to locate earthquakes. Due to the Pn (Sn) spreading distance is far, the traveling time of the seismic phase is easily affected by lateral heterogeneity of medium. Seismic location based on Pg (Sg) phase can only obtain high precision focal depth when the number of near stations is sufficient and the station azimuth coverage is good. Under the circumstances of the seismic network relatively sparse, due to the lack of sufficient near station data, the accuracy of focal depth determined by conventional positioning methods is low. At present, the layout of most stations in China is relatively sparse, so the deep seismic phase method will have a better effect.

According to CENC, an Ms 5.2 earthquake occurred in Qilian County, Haibei Tibetan Autonomous Prefecture, Qinghai Province(37.65°E, 101.62°N) on 5:2:42, November 23, 2015 (GMT+8), with a focal depth of 10km. Earthquakes are felt in many places in Qinghai and Gansu, earthquakes have a greater effect on the Qilian County of Qinghai Province and Sunan County of Gansu Province. Earthquakes occurred in the Qilian fault zone and its styles mainly are large sinistral strike-slip faults.

2 Regional tectonic background and aftershock distribution

The Haiyuan fault imitates at the Hala lake in the Qilian Shan to the west, goes through the Menyuan county of Qinghai Province, Jingtai county of the Gansu Province and Haiyuan county of the Ningxia Hui autonomous region eastward, terminates at south of Zhongwei county at the most east, and merge into Liupan Shan uplift area. The east section of the Haiyuan fault is a boundary of Qilian and Alxa blocks, slips left-laterally with vertical motion locally. Strong earthquakes occurred in the north of the Lenglongling section in recent years. Because of the Tibet plateau expansion northward, the Qilian Shan has been shortened and uplifted and formed a long banded Range-Basin feature. There are many minor thrusts with weak horizontal slip in this area, such as Danghe Nanshan fault, Shule Nanshan fault, central Qilian Shan fault, Yemahe fault, north Qilian Shan fault, and Fodongmiao-Hongyazi fault. There are also many minor faults distribute along the Hexi corridor, including Yumen fault, Jiyuguan fault, Helishan fault, Jinta Nanshan fault, Yumu Shan fault, Dahuang Shan fault, Longshou Shan fault, Shandan-Minle blind fault, and Gulang thrust. Fig 1 shows that aftershocks distributes with the trending of SE-NW.
3 CAP method brief introduction and calculation results

3.1 Brief introduction to the CAP method

The CAP method is a full waveform inversion method compared with the previous P-wave first motion, body wave inversion or surface wave inversion. It divides broadband seismic records into Pnl and surface waves for inversion and allows them to float relatively, gain the focal mechanism solution with the smallest global difference between synthetic seismogram and observed seismogram within the appropriate time range. The CAP method has the characteristics of fewer requirements for the number of stations involved in inversion, azimuth distribution does not need to be very uniform, inversion results are less dependent on the velocity model and the lateral in homogeneity of crustal structure. At present, some research results fully prove the validity and reliability of the CAP method in focal mechanism solution and seismic centroid depths research [1-3].

The main principle of the CAP method is: the theoretical synthetic displacement s(t) of any double-couple source can be expressed as formula (1).

\[
s(t) = M_0 \sum_{i=1}^{3} A_i (\theta - \phi_i, \delta, \lambda) G_i(t) \tag{1}
\]

In the formula, i=1,2,3 respectively corresponds to three basic fault types: vertical strike-slip, vertical dip-slip, and 45° dip-slip; G_i is Green function, A_i is ray coefficient, \( \theta \) is station azimuth angle, \( M_0 \) is scalar moment; \( \phi_i, \delta, \lambda \) respectively represents the direction, dip and slip angle of the obtained focal mechanism solution.

In the process of inversion, the synthetic seismic displacement s(t) and observed seismic displacement u(t) are consistent is taken as the judge criterion, as shown in formula (2)

\[
u(t) = s(t) \tag{2}
\]

An error objective function can be defined to measure the difference between s and u:

\[
e = \left\| \left( \frac{r}{r_0} \right)^P \cdot [u - s] \right\| \tag{3}
\]

In the formula (3), \( r \) is the epicentral distance, \( r_0 \) is the selected reference epicentral distance, \( P \) is an exponential factor being adopted considering the influence of geometric diffusion factor on the seismic waveform, it makes the moment magnitude of earthquakes comparatively reliable. In reference to previous research experience [4], in general, body wave inversion \( P=1.0 \), surface wave inversion \( P=0.5 \).

The method divides the broadband seismic records into Pnl and surface waves to inversion focal mechanism solution. The focal mechanism solution with the smallest global difference between synthetic seismogram and observed seismogram is searched in an appropriate time range, which enhances the weight of Pnl and has better constraints on seismic depth.

3.2 Data processing and calculating results

We select the waveform records of 16 broadband digital seismic stations in the regional seismic network of Gansu province, Qinghai province, and Sichuan province [5-6] involved inversion, the distribution of seismic stations is shown in Fig 3, maximum station field angle is 42.4°. The epicenter distance is in the range of 50km~600km, and the waveform records have a higher signal-to-noise ratio. The used seismograph types include BBVS-60, CMG-3ESPC, CTS-1, BBVS-120, etc. The observation frequency band is 60 s~50 Hz or 120 s~50 Hz, sampling rates all are 100 Hz. The digital seismic data with a high signal-to-noise ratio have laid a good foundation for this study. All data was processed by remove mean, eliminate the responses of instruments, normalization, and filtering. We select the CRUST 2.0 global velocity model table 1 as the velocity model. The final results (see table 2) agree with the IGP-CEA results.

![Fig. 1. Aftershock distribution.](image)

### Table 1. Velocity model.

| Layer number | Thickness/ km | Vp/km·s⁻¹ | Vs/km·s⁻¹ |
|--------------|---------------|---------|--------|
| 1            | 0.5           | 2.5     | 1.2    |
| 2            | 18            | 6.1     | 3.5    |
| 3            | 16            | 6.3     | 3.6    |
| 4            | 9.5           | 7.2     | 4.0    |
| 5            | 0             | 8.0     | 4.6    |
4 The sPn seismic phase identification and depth calculation

The sPn phase is a practical seismic phase for determining the focal depth of shallow earthquakes with short distance (Δ<1000km). Assuming that the source is not on the surface (h≠0) and to simplify the description, the crust is simplified as a double layer (Fig. 5).

When an earthquake occurs in the earth's crust, S-wave rays incident on the earth's surface, reflect and convert to P-wave and then incident to Moho surface. When the incident angle is critical, the Pn wave is formed, since it is converted from S wave, it is denoted as sPn wave and its ray propagation path see Fig. 5. Although the sPn wave keeps the dynamics characteristics of the shear wave and the amplitude and period are larger than that of the longitudinal wave, they appear in the seismic record in the form of a longitudinal wave. Therefore, the vertical direction is displayed, and the amplitude and period of the shear wave are larger than that of Pn. The sPn phase appears between Pn and Pg. The paper using a double-layer seismic model theory calculates the arrival time difference between sPn and Pn.
Fig. 5. Propagation path of sPn seismic phase from the double-layered crustal model.

vs1 and v1 represent the propagation velocities of S and P waves in the upper crust, respectively. v3 represents the propagation velocity of internal waves in the lower crust, that is, the propagation velocity of the Pn wave; the h is focal depth. The arrival time difference of Pn wave can be deduced from the Snell law,

\[ \Delta t = h \left( \frac{\sqrt{v_3^2 - v_{s1}^2}}{v_3 \cdot v_{s1}} + \frac{\sqrt{v_3^2 - v_1^2}}{v_3 \cdot v_1} \right) \quad (4) \]

According to the crustal model of travel time difference of seismic wave in Gansu area [7-8], it can be deduced:

v1=6.09km/s, vs1=3.56km/s, v3=8.17km/s, then K=2.757. That is the depth of the source in the upper crust: h=2.757 \( \Delta t \). The phase characteristic of sPn is that the arrival time difference independent of epicentral distance and only related to the focal depth. According to this property of the sPn phase, if moving the Pn phase of different epicentral distances to a line in the same time window, the sPn phase is also coming into a line. In this way, the sPn phase can be determined accurately and quickly, and then the focal depth can be determined. Fig 6 is Phase analysis from waveform. Waveform is processed by low-pass 1Hz filtering. Station waveforms are arranged in order of epicentral distance is ZHW, XSH, LQT, LTT, HYU, MXT, JNT, GYU, JYU. The transverse axis is coming into a line according to Pn phase, longitudinal axis distribution according to epicentral distance; it can be seen from the Fig 6 that the average the arrival time difference between sPn and Pn is about 2.48S. These parameters are substituted into the formula (1) obtained depth is 6.6 km. Comparisons with CAP results of 8km, the error range is 1.4 km, the gap between the two results is very small.

Fig. 6. Phase analysis from waveform.

5 Conclusion and Discussion

In this paper, we select 16 seismic stations waveform records to invert the M5.2 Qilian earthquake by using CAP focal mechanism solution method. Combined with the tectonic background and aftershock distribution characteristics in Qilian area, determine the main axis parameters of the strike is 112°, the dip, 51.7° and the rake, 24.5°, there was a left-lateral strike-slip fault with thrust property and optimal depth solution is 8 km, the results agree with the IGP-CEA results. Based on the results of the focal mechanism and tectonic background of the Qilian region, it is concluded that the causative structure of this earthquake is a boundary fault zone between Qilian Mountain block and Alxa block in the eastern segment of Haiyuan fault. To compare the results of focal depths, this paper used the depth phase sPn method. Calculate the focal depth with the arrival time difference between sPn and Pn phases, the results of 6.6km is consistent with the CAP method results of 8km. The focal depth of this earthquake is determined to be about 6-8km. The reliability of this method is verified by comparing it with the optimal depth solution of the CAP focal mechanism and other research institution’s results.

The seismic waveform data used in this paper are from the Gansu Digital Seismic Network. All the charts in this paper are drawn by SAC, GMT and Matlab software.

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