A history of the gamma-ray burst flux at the Earth from Galactic globular clusters

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ABSTRACT

Nearby gamma-ray bursts (GRBs) are likely to have represented a significant threat to life on the Earth. Recent observations suggest that a significant source of such bursts is compact binary mergers in globular clusters. This link between globular clusters and GRBs offers the possibility to find time intervals in the past with higher probabilities of a nearby burst, by tracing globular cluster orbits back in time. Here we show that the expected flux from such bursts is not flat over the past 550 Myr but rather exhibits three broad peaks, at 70, 180 and 340 Myr ago. The main source for nearby GRBs for all three time intervals is the globular cluster 47 Tuc, a consequence of its large mass and high stellar encounter rate, as well as the fact that it is one of the globular clusters that come quite close to the Sun. Mass extinction events indeed coincide with all three time intervals found in this study, although a chance coincidence is quite likely. Nevertheless, the identified time intervals can be used as a guide to search for specific signatures of GRBs in the geological record around these times.

Key words: astrobiology – gamma-ray burst: general – globular clusters: general – Galaxy: kinematics and dynamics.

1 INTRODUCTION

Globular clusters, densely packed groups of old stars, can efficiently produce close stellar binaries by dynamical interactions of their member stars. Examples for such dynamically formed binaries include low-mass X-ray binaries (e.g. Clark 1975; Katz 1975), cataclysmic variables (Pooley & Hut 2006) and millisecond pulsars (msPSRs; Ransom 2008; Abdo et al. 2010). The most extreme binaries found in globular clusters consist of two neutron stars (Anderson et al. 1990). Mergers of such binaries are believed to be the central engine of short gamma-ray bursts (GRBs; Grindlay, Portegies Zwart & McMillan 2006; Dado, Dar & De Rujula 2009; Lee, Ramirez-Ruiz & van de Ven 2010), which produce brief, intense flashes of ionizing radiation. In contrast to short bursts, long bursts are believed to originate from the death of short-lived massive stars (see Gehrels, Ramirez-Ruiz & Fox 2009 for a review on long and short bursts). It has been argued that the rate of short GRBs in the local Universe is dominated by the merger of neutron star binaries formed in globular clusters (Salvaterra et al. 2008; Guetta & Stella 2009). A link between globular clusters and short GRBs is further supported by the presence of a short GRB remnant candidate in the Galactic globular cluster Terzan 5 (Domainko 2011a), observed in the very high energy gamma-ray (Abramowski et al. 2011, 2013), X-ray (Eger, Domainko & Clapson 2010; Eger & Domainko 2012) and radio waveband (Clapson et al. 2011). Additional evidence for the GRB–globular cluster connection comes from spatial offsets of short GRBs from their host galaxies (Berger 2010; Salvaterra et al. 2010; Church et al. 2011) and the redshift distribution of such events (Salvaterra et al. 2008; Guetta & Stella 2009).

Since globular clusters follow well-defined orbits around the Galaxy (Domainko 2011b), their coupling with GRBs allows us to examine the longstanding question of the past history of gamma-ray flux on the Earth. [A similar approach for supernovae (SNe) exploding in star clusters has been used in Svensmark (2012)]. Numerous studies have shown that gamma-rays from SNe or GRBs could, in principle, have had a significant impact on the Earth’s atmosphere and biosphere, potentially even contributing to mass extinctions (see Thorsett 1995; Scalo & Wheeler 2002; Melott et al. 2004; Thomas et al. 2005 for the effect of GRBs in general, and Dar, Laor & Shaviv 1998; Melott & Thomas 2011 for the effect of merger-induced bursts). However, demonstrating that SNe or GRBs may in fact have played some role first requires identifying that sources could have come near enough to the Earth at some point. Some previous studies have attempted to make a connection between the solar motion relative to the Galactic plane and spiral arms, on the assumption that the gamma-ray flux incident on the Earth is larger in these regions of enhanced massive star formation rate and/or increased stellar density (see Bailer-Jones 2009 for a review). However, a recent study shows that the flux from these
sources as modulated by the plausible solar motion over the past 550 Myr has a poor correlation with the variation of the extinction rate on the Earth (Feng & Bailer-Jones 2013).

Indeed, it seems that astronomical phenomena alone are unlikely to be the dominant driver of biological evolution or the cause of all (or even most) mass extinctions. Nonetheless, if a GRB were to explode near the Earth, its consequences could be catastrophic, and globular clusters are presumably a significant source of GRBs.

The goal of this paper is to reconstruct the orbits of globular clusters relative to the Sun in order to calculate the GRB flux at the Earth as a function of time, and thereby to identify potential candidate clusters. The data for this orbital reconstruction come from the positions, distance, proper motion and radial velocity catalogues of globular clusters of Dinescu et al. (1997, 1999a, 2003) and Dinescu, Girard & van Altena (1999b), from which we obtain the current Galactic coordinates and space velocities. By sampling over the (often significant) uncertainties in the reconstructed orbits of the globular clusters and the Sun, we infer the expected GRB flux as a function of time. This allows us to identify the most probable intervals in the Earth’s history of a significantly increased gamma-ray flux, which may (or may not) be associated with times of higher extinction rate.

In Section 2.1, we describe the orbital reconstruction method, and in Section 2.2 we explain how we derive from this the probability distribution over the past cluster–Sun separation and the expected gamma-ray flux at the Earth. This takes into account the different GRB rates in the clusters, which are derived in Section 2.3. We give our results in Section 3 where we also identify some past extinction events. We conclude in Section 4 with an outlook on how to further this work.

2 METHODS

2.1 Reconstructing Galactic orbits

We trace the orbits of the Sun and the globular clusters back in time by integrating the equations of motion through the Galactic potential. In a purely gravitational system, there is no dissipation of energy, so the dynamics are reversible. We adopt an analytic, three-component, axisymmetric potential, $\Phi$, comprising the Galactic bulge, halo and disc

$$\Phi(R, z) = \Phi_b + \Phi_h + \Phi_d. \quad (1)$$

The bulge and halo are represented with a Plummer distribution

$$\Phi_{b,h} = \frac{-G M_{b,h}}{\sqrt{R^2 + z^2 + b^2_{b,h}}} \quad (2)$$

in which the characteristic length scale is $b_h = 0.35$ kpc for the bulge and $b_b = 24.0$ kpc for the halo, and the bulge and halo masses are $M_b = 1.40 \times 10^{10} M_\odot$ and $M_h = 6.98 \times 10^{11} M_\odot$ respectively. $R$ is the radial coordinate perpendicular to the axis and $z$ is the distance from the Galactic plane. For the disc we use the potential from Miyamoto & Nagai (1975)

$$\Phi_d = \frac{-G M_d}{\sqrt{R^2 + (a_d + \sqrt{z^2 + b^2_d})^2}} \quad (3)$$

with the values $M_d = 7.91 \times 10^{10} M_\odot$ for the disc mass, and $a_d = 3.55$ kpc and $b_d = 0.25$ kpc for the scalelength and scale height of the disc, respectively (after García-Sánchez et al. 2001). The integration is performed numerically from the present back to 550 Myr before present (BP). This time limit is chosen because it corresponds to the beginning of the Phanerozoic eon, a time from which the fossil record becomes more indicative of biodiversity variations. The globular clusters (and Sun) are treated as massless.

The initial conditions for the integration are the current phase space coordinates (three position and three velocity components) of the globular clusters (and Sun). These of course have significant uncertainties, each represented as a Gaussian with known mean (measured coordinate) and standard deviation (estimated uncertainty). These come from Dana Casetti-Dinescu’s catalogue for globular cluster’s three-dimensional space velocities (2012 version) for the globular clusters and from Hipparcos data by Dehnen & Binney (1998) for the Sun. We further use a distance of the Sun to the Galactic centre obtained from astrometric and spectroscopic observations of the stars near the supermassive black hole of the Galaxy (Eisenhauer, Schödel & Genzel 2003), and the displacement of the Sun from the Galactic plane is calculated from the photometric observations of classical Cepheids by Majaess, Turner & Lane (2003). Rather than just performing a single integration for each object (cluster or Sun), we Monte Carlo sample its initial conditions from the uncertainty distribution in order to build up a large sample of orbits. Fig. 1 shows an example of such sample orbits for one globular cluster, 47 Tuc, by plotting the distance of the cluster from the Sun over time. (We sample over the possible orbits of the Sun too.) We do not take into account the (possibly significant) uncertainties in the Galactic potential. In principle, we could adopt an uncertainty model for these parameters and marginalize over them also. But we choose to omit this in this first investigation.

Finally, we have to note that compact binaries may be ejected from their parent cluster before they merge and produce a GRB (e.g. Phinney & Sigurdsson 1991; Ivanova et al. 2008). This effect will smear out the distribution of compact binaries around the producing cluster. The typical escape velocities for massive globular clusters are about 50 km s$^{-1}$, which is comparable to the present uncertainties of the globular cluster velocity. Although over time the orbit of the ejected binary could deviate considerably from its parent cluster, the uncertainty in its orbit is comparable to the uncertainty for its parent cluster, which we take into account. Therefore

\[ http://www.astro.yale.edu/dana/gc.html \]
choose to omit the issue of ejected GRB progenitors for this first investigation. Furthermore, more massive clusters are better able to retain their binaries, and these are the clusters that preferentially produce GRBs (see Section 2.3).

### 2.2 The probability distribution over globular cluster distances and the expected GRB flux at the Earth

For a given globular cluster, \( c \), we convert the set of (thousands of) relative orbits into a two-dimensional density distribution over time, \( t \), and separation, \( r \), using kernel density estimation. We interpret the resulting distribution as a probability distribution of the Sun–cluster separation over time, \( f_c(r, t) \), which is normalized such that \( \int_0^\infty f_c(r, t) \, dr = 1 \) for all \( t \) and for each cluster. This is shown in Fig. 2 for 47 Tuc, in which the probability density is plotted as a grey-scale. At any given time, the darker the band, the more concentrated the probability is around a smaller range of distances. The width of the distribution at any time is determined by how the uncertainties in the present coordinates of both globular cluster and Sun propagate back in time. The density estimates for some other globular clusters are shown in Figs 3–7.

The flux of a GRB at the Sun is proportional to \( 1/r^2 \). Multiplying \( f_c(r, t) \) by \( 1/r^2 \), and assuming that GRBs occur at random times,\(^2\) we get a 2D distribution which is proportional to the expected GRB flux from distance \( r \) at time \( t \). If we integrate this (at a time \( t \)) over \( r \), the result is the probability per unit time of a burst for each globular cluster.

\(^2\) GRBs are of course discrete, rare events. Lacking information on when they occurred, the best we can do is to derive the probability per unit time of a burst for each globular cluster.
over all distances, then we get a quantity, \( \int f_c(r,t) dr \), which is proportional to the expected GRB flux from that globular (at time \( t \)). The important thing about this quantity is that it takes into account the uncertainties in the reconstructed globular cluster and solar orbits.

We now extend this concept to the complete set of globular clusters. Each cluster has a different probability per unit time of producing a GRB, proportional to the factor \( w_c \), defined in Section 2.3. We can then see that the quantity

\[
\Psi(t) = \int_{r=0}^{r_{\text{max}}} \sum_c w_c \frac{1}{r^2} f_c(r,t) \, dr
\]

is proportional to the expected GRB flux at the Sun at time \( t \) from any globular cluster. In principle, we integrate up to \( r_{\text{max}} = \infty \), but in practice we can truncate it to a few kpc. Indeed, if there is a minimum flux threshold below which the gamma-ray flux is too small to have any significant effect on the Earth’s biosphere or climate, then truncation is appropriate. Note that the absolute scale of \( \Psi(t) \) is not calibrated: only relative values are meaningful.

### 2.3 Weighting individual globular clusters

Observationally, the frequency of occurrence of GRBs in individual globular clusters is not known. The dynamical formation of compact binaries, proposed progenitors of such events, is rather complex, involving at least two stellar encounters (see Ivanova et al. 2008, 2010). However, the rate of GRBs in each globular cluster is expected to be linked to the cluster properties. Several authors have already investigated the dependence of the compact binary formation rate on the characteristics of the clusters. Ivanova et al. (2008) found that the formation of close double neutron star binaries depends on the square of the cluster density, and that the number of retained neutron stars increases as the escape velocity (and thus cluster mass) increases. Grindlay et al. (2006) used a model where the formation of double neutron star binaries scales linearly with the neutron star number density, the velocity dispersion (and thus mass of the cluster) and the number of potential progenitor systems (binaries containing one neutron star). Both models find that massive clusters with a high concentration of stars strongly favour the formation of prospective GRB progenitor systems. Here we adopt a similar approach to these previous works and scale the expected GRB rate with quantities that are known for a large sample of globular clusters.

Specifically, assuming that GRBs are caused by neutron star encounters, the GRB rate will depend on the number of neutron stars in the cluster and their encounter rate. We assume that the number of neutron stars scales linearly with the mass of the globular cluster, \( m_c \), and thus linearly also with the cluster luminosity. The total encounter rate, \( \Gamma_c \), is given as \( \Gamma_c \propto \rho_0^{\frac{3}{5}} r_{\text{core}}^2 \) (Pooley & Hut 2006), where \( \rho_0 \) is the central stellar number density and \( r_{\text{core}} \) is the core radius of the globular cluster. Values for these parameters for our sample of clusters we obtained from Harris (1996, 2010 edition). Combining these two factors we get a quantity \( w_c = m_c \Gamma_c \), which is proportional to the frequency of GRBs in the clusters and is used as the weighting factor in Section 2.2. Accordingly, and as already noted in the beginning of this section, massive clusters with high concentrations of stars at their centre have a large GRB rate. We investigated the uncertainties of our approach by applying an alternative weighting scheme for individual globular clusters. We followed Ivanova et al. (2008) and adopted weights proportional to \( \rho_0^2 m_c \). With this approach we found that the typical uncertainties for the leading clusters are a factor of a few, with a few notable exceptions (see Section 3). For the results in Section 3, we use the weights \( w_c \) as defined earlier in this section.

Having calculated the individual weights, \( w_c \), they are then normalized such that the sum of all weights equals 1. Here we used 141 clusters from Harris (1996, 2010 edition) where all necessary parameters are known. This, in principle, further allows us to estimate the expected absolute GRB rates for individual globular clusters by defining that a weight of 1 corresponds to the Galactic rate of GRBs launched in globular clusters. This galactic GRB rate can be calculated from the short GRB rate in the local Universe of \( 8.3 \pm 3 \) Gpc\(^{-3} \) yr\(^{-1} \) (Coward et al. 2012) and the density of Milky Way-type galaxies of 0.01 Mpc\(^{-3} \) (Cole et al. 2001). This rate is obtained for GRBs beamed towards Earth and is thus independent of the degree of collimation of the events. If it is assumed that the occurrence of short GRBs in the local Universe is dominated by bursts launched in globular clusters (Salvaterra et al. 2008; Guetta & Stella 2009), then the combined GRB rate of all globular clusters is \( 10^{-6} \) yr\(^{-1} \). This estimate is also consistent with the theoretically expected rate of short GRB production in these clusters (Lee et al. 2010).

### 3 RESULTS

Fig. 8 shows the expected GRB flux, \( \Psi(t) \), for the case \( r_{\text{max}} = 5 \) kpc. This distance threshold covers 95 per cent of all hazardous GRBs if a log-normal GRB luminosity distribution with \( \log E_{\gamma,\text{iso}} = 50.81 \pm 0.74 \) erg (Racusin et al. 2011) and a critical fluence at Earth for a significant effect on the biosphere or climate of \( 10^4 \) erg cm\(^{-2} \) (Melott & Thomas 2011) is assumed. (The profile of \( \Psi(t) \) has very similar shape for other values of \( r_{\text{max}} \), the difference being that the ‘background’ level is higher for larger values of \( r_{\text{max}} \) and lower for smaller values.) We see a significant variation. There are three broad peaks, at 70, 180 and 340 Myr. These correspond to times in the Earth’s history when – within the limitations of our orbital reconstruction and assumptions made – we would expect a significantly higher level of GRB flux than the average over the past 550 Myr.

Examining the plots of \( f_c(r,t) \) for all clusters, we can identify those clusters which make the biggest contribution to \( \Psi(t) \) in each peak.

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3 http://physwww.mcmaster.ca/~harris/mwgc.dat
The expected GRB flux, $\Psi(t)$, at the Sun as a function of time BP in arbitrary units. The vertical lines denote the times of the 18 mass extinctions events compiled by Bambach (2006).

(i) Peak at 70 Myr. The main contributor is 47 Tuc, which has 10 times the contribution to $\Psi(t)$ than does the next cluster, NGC 1851.

(ii) Peak at 180 Myr. The main contributor is again 47 Tuc, with several others contributing at a level 5–20 times lower, the largest of these being Omega Cen, M13 and M15.

(iii) Peak at 340 Myr. Once again 47 Tuc gives the largest contribution, with several others contributing at a level seven or more times lower, the most significant of these being NGC 2808.

The prominence of 47 Tuc is a consequence both of its high weight, $w_c$, and the fact that it is one of the globular clusters that come quite close to the Sun. All the main contributors are massive clusters that contain significant populations of dynamically formed stellar binaries. Specifically:

(i) 47 Tuc has the second largest number of radio-detected msPSRs (23; Ransom 2008), detected by Fermi-LAT in high-energy gamma-rays (Abdo et al. 2010). In our weighting scheme (see Section 2.3), it would account for about 5 per cent of the GRBs produced in globular clusters. In the alternative weighting scheme (see Section 2.3), it accounts for about 1 per cent of GRBs in globular clusters (for the following clusters, this number is given in parentheses). 47 Tuc is the dominant globular cluster in our study for both weighting schemes.

(ii) NGC 1851 contains an msPSR in a very eccentric binary system with massive secondary (Feire et al. 2004). This could account for about 2 per cent (1 per cent) of GRBs from globular clusters.

(iii) NGC 2808 is a massive globular cluster with complex evolutionary history (Piotto et al. 2007). This could account for about 5 per cent (0.3 per cent) of GRBs from globular clusters.

(iv) Omega Cen is the most massive globular cluster in the Galaxy, detected by Fermi-LAT (Abdo et al. 2010). This could account for about 2 per cent ($10^{-3}$ per cent) of GRBs from globular clusters. For this globular cluster, the two different weighting schemes give the largest difference since it is a very massive cluster with a shallow density profile.

(v) M13 contains five radio-detected msPSRs (Ransom 2008). This could account for about 0.2 per cent ($10^{-3}$ per cent) of GRBs from globular clusters.

(vi) M15 has a double neutron star binary that will merge within a Hubble time (Anderson et al. 1990) and eight radio-detected msPSRs (Ransom 2008). This could account for about 6 per cent (2 per cent) of GRBs from globular clusters.

As mentioned earlier, GRBs are of course discrete, rare events. Indeed, our calculations suggest that only about 10 GRBs will have occurred within 5 kpc of the Sun over the course of the Phanerozoic. Thus, the true distribution of flux with time would comprise a series of narrow peaks of various heights. Fig. 8 shows the expected flux as a function of time (multiplied by a constant), so is the best single estimate of that distribution.

By way of comparison we overplot in Fig. 8 the times of 18 mass extinction events on the Earth revealed by the fossil record, as compiled by Bambach (2006). One may be tempted to draw a causal connection between one of these events and one of the peaks in $\Psi(t)$, although clearly there is a reasonable chance that one of these 18 events could coincide with a peak just by chance. It is nonetheless worthwhile identifying those events nearest to the three peaks. These are

(i) Peak at 70 Myr: the famous KT extinction at 65 Myr BP, generally accepted to have had a significant role in the demise of the dinosaurs;

(ii) Peak at 180 Myr: the late Pliensbachian/early Toarcian (early Jurassic) extinction event at 179–186 Myr BP;

(iii) Peak at 340 Myr: the early Serpukhovian (mid-Carboniferous) extinction event at 322–326 Myr BP, and the late Famennian (late Devonian) extinction event at 359–364 Myr BP.

Whether or not a globular cluster GRB is implicated in any of these extinctions remains a subject for future work.

4 OUTLOOK

In this paper, we have traced globular cluster orbits back to the beginning of the Phanerozoic eon in order to identify time intervals where a high flux of ionizing radiation caused by a nearby GRB is more likely. We found that the probability for such an event is far from flat with time during the Earth’s history. It instead exhibits several distinct peaks, the most prominent ones being around 70, 180 and 340 Myr BP. The main source of GRBs in all cases is 47 Tuc. All three time intervals can in principle be associated with a mass extinction event, although a chance coincidence is likely. Therefore, to establish a link between a nearby GRB and an impact on the Earth and its biota, supporting geological signatures are needed. Geological signatures could comprise radiation damage of crystals [e.g. fossil cosmic ray tracks (Fleischer et al. 1967) or colour shifts (Ashbaugh 1988)], deposition of radioactive isotopes (Dar et al. 1998) or elevated rates of bone cancer (Rothschild et al. 2003). The time intervals identified in this paper can be used as a guideline to search for such signatures in the geological record.

Finally, the current orbital parameters of globular clusters and the Solar system are subject to considerable uncertainties. (These were taken into account in our analysis, and contribute to smearing out the probability curve.) This situation will be substantially improved in the near future with the launch of the Gaia satellite, which will determine the dynamics of the Galaxy with unprecedented accuracy. With better determined orbital parameters we will be able to constrain the past orbits more tightly, and so repeat this study to give results of higher confidence.

The probability that any one event, thrown down at random over the time range 0–550 Myr, would not land in a particular box of width 20 Myr [the width of the peaks in $\Psi(t)$] is $1 - 20/550 = 0.5$. So the probability that at least one of the 18 events coincides with such a box just by chance is $1 - (1 - 20/550)^{18} = 0.5$. This is not a proper hypothesis test, but it highlights that a coincidence is quite likely.
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