Internal Water and Microsecond Dynamics in Myoglobin
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Abstract: Myoglobin (Mb) binds diatomic ligands, like O₂, CO, and NO, in a cavity that is only transiently accessible. Crystallography and molecular simulations show that the ligands can migrate through an extensive network of transiently connected cavities but disagree on the locations and occupancy of internal hydration sites. Here, we use water ²H and ¹⁷O magnetic relaxation dispersion (MRD) to characterize the internal water molecules in Mb under physiological conditions. We find that equine carbonmonoxy Mb contains 4.5 ± 1.0 ordered internal water molecules with a mean survival time of 5.6 ± 0.5 μs at 25 °C. The likely locations of these water molecules are the four polar hydration sites, including one of the xenon-binding cavities, that are fully occupied in all high-resolution crystal structures of equine Mb. The finding that water escapes from these sites, located 17–31 Å apart in the protein, on the same μs time scale suggests a global exchange mechanism. We propose that this mechanism involves transient penetration of the protein by H-bonded water chains. Such a mechanism could play a functional role by eliminating trapped ligands. In addition, the MRD results indicate that 2 or 3 of the 11 histidine residues of equine Mb undergo intramolecular hydrogen exchange on a μs time scale.

1. Introduction
The 153-residue hemoprotein myoglobin (Mb) transports O₂ from sarcolemma to mitochondria in cardiac and skeletal muscle tissue of most mammals.

Despite a large amount of experimental and computational work,

The permanent cavities in Mb, with a combined (probe-size-dependent) volume approaching 300 Å³, could accommodate a dozen water molecules, but since most of them are lined by non-polar side chains, one expects a low water occupancy. Indeed, high-resolution crystal structures of Mb have identified only four (equine Mb)

The water MRD technique measures the magnetic field (or resonance frequency) dependence of the longitudinal spin relaxation rate R₁ of one of the magnetic water nuclides ¹H, ²H, or ¹⁷O.

Two of the MRD studies employed the ¹H nuclide to determine the paramagnetic relaxation enhancement for the DP water in met-Mb. The more recent MRD study, which used the ²H and ¹⁷O nuclides, concluded that equine MbCO contains at least three internal water molecules with survival times exceeding the ~10 ns tumbling time of Mb.

From MRD measurements on protein solutions, one can obtain the number of water molecules with a survival time longer than a lower bound set by the protein tumbling time (~10 ns for Mb) and shorter than an upper bound set by the intrinsic spin relaxation rate for the internal water molecule (~1 μs for ¹⁷O and ~100 μs for ²H).

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rather wide range, solution MRD experiments cannot differentiate water molecules with different survival times.

More information can be obtained if the protein is immobilized by a chemical cross-linking reagent such as glutaraldehyde (GA) so that molecular tumbling is inhibited. The MRD profile is then essentially the Fourier transform of the survival correlation function, and survival times up to ~10 μs of individual internal water molecules can be determined directly from the 2H MRD profile.

Here, we report an extensive set of 2H and 17O MRD data from equine MbCO. Water dynamics on the ns to μs time scale is characterized in detail by examining solutions with free-tumbling Mb as well as cross-linked gels with immobilized Mb, in both cases under fully hydrated conditions (~1.6 mM Mb). To extract quantitative information about internal water molecules from 2H MRD data, it is necessary to isolate any contribution from rapidly exchanging labile deuterons in the protein. By analyzing the pD dependence of the 2H MRD and by comparing with the 17O MRD, we find that several histidine side chains in Mb exchange deuterons with water on the μs time scale, apparently by an intramolecular catalytic mechanism involving an adjacent deuteron exchange catalyst, such as a carboxylate.

The principal questions that we address here are the following: (1) How many internal water molecules occupy the internal cavities of Mb under physiological conditions? (2) Where are they located? In particular, are the Xe binding sites hydrated? (3) How long do the internal water molecules remain inside the cavity network? (4) By what mechanism do the internal water molecules exchange? (5) Does the internal water play a purely structural role, or are they involved more directly in the function of Mb?

2. MATERIALS AND METHODS

2.1. Sample Preparation. Lyophilized equine skeletal muscle Mb was purchased from Sigma (≥95%) and further purified by cation-exchange chromatography (SP sepharose; GE Healthcare). The purified Mb was lyophilized following extensive dialysis against Milli-Q water. To prepare carbon-monoxo Mb (MbCO) samples, the purified protein was dissolved in 99.8% D2O (Cambridge Isotope Laboratories) with (gel samples) or without (solution samples) a buffer. For 17O MRD experiments, 20% 17O-enriched D2O was used. By using D2O for both 2H and 17O MRD experiments, correlation times can be compared directly without correcting for the unknown H/D kinetic isotope effect.

The solution was centrifuged at 13 000 rpm for 3 min to remove any insoluble protein, flushed with CO gas for 3 min on ice, and equilibrated by stirring for 30 min at 6 °C. Mb was then reduced by adding ~2 equiv of sodium dithionite (Sigma), and the process of flushing CO gas for 2–3 min and stirring for 30 min was repeated (usually five times) until no further change in the optical absorption spectrum could be detected (Shimadzu UV-1800). The Mb concentration was determined from the absorbance at 542 nm with an extinction coefficient, 18.4 mM−1 cm−1, that had been calibrated using complete amino acid analysis (performed at Amino Acid Analysis Center, Dept. of Biochemistry and Organic Chemistry, Uppsala University, Sweden). MRD measurements were performed on seven solution samples with 2.0–2.6 mM Mb and on 26 gel samples, 23 of them with 1.6–1.7 mM Mb (Table S1, Supporting Information).

The protein was immobilized by adding 25% GA solution (Sigma) to the MbCO solution at 6 °C.64 Except for two cases (Table S1, Supporting Information), the Ga/Mb mole ratio, NGa,Mb, was in the range 29.7–31.1. After mixing by pipetting, an aliquot (~50 μL) of the solution was removed for pH measurement and the remainder was transferred to a glass tube (8 mm o.d. × 12 mm height), where it was cross-linked overnight at 6 °C. For the solution samples, pH was adjusted by adding either HCl or NaOH. Reported pH values are corrected for the H/D isotope effect according to pH = pH* + 0.41, where pH* is the reading on a pH meter calibrated with H2O buffers.

To pressurize Xe in a cross-linked MbCO sample, the protein was immobilized in a 10 mm heavy wall NMR tube with a pressure/vacuum valve (Wilmad). After cross-linking, the NMR tube was filled with 8 bar of Xe gas (AGA, Sweden) and equilibrated for 1 week before NMR experiments. To estimate the Xe concentration in the MbCO sample, two reference samples (cyclohexane and 50 mM PIPES pD 7.4 in D2O) were prepared. The reference solutions were placed in 10 mm NMR tubes, and Xe gas was bubbled through the liquid.

2.2. NMR Experiments. The water 2H or 17O longitudinal relaxation rate, R1, was recorded on six different NMR setups: (1) a Stelar Spinmaster 1 T fast field-cycling (FC) spectrometer (2H, 1.5 kHz to 5.4 MHz); (2) a Tecmag Apollo console equipped with a GMW field-variable (±1.8 T) iron-core magnet (17O, 0.7–1.6 MHz); (3) a Tecmag Discovery console
equipped with a Drusch field-variable (≤2.1 T) iron-core magnet (\(^{2}H, 2.5–13.1 \text{ MHz}; ^{17}O, 2.2–11.5 \text{ MHz}\)) or (4) with a Bruker 4.7 T superconducting magnet (\(^{2}H, 30.7 \text{ MHz}; ^{17}O, 27.1 \text{ MHz}\)); and (5) Varian DirectDrive 600 (\(^{17}O, 67.8 \text{ MHz}\)) and (6) 600 (\(^{2}H, 92.1 \text{ MHz}; ^{17}O, 81.3 \text{ MHz}\)) spectrometers. For the \(^{2}H\) FC measurements, pre-polarized single-pulse (≤2.6 MHz) or inversion recovery (>2.6 MHz) sequences were used with pre-polarization and detection at 5.4 and 4.8 MHz, respectively. On other spectrometers, the standard inversion recovery pulse sequences were used. 125Xe spectra were recorded on a Varian DirectDrive 600 (125Xe, 166 MHz) using a single 90° pulse. All NMR experiments were performed at 25.0 ± 0.1 °C, maintained by a thermostatted air flow. The sample temperature was checked with a thermocouple referenced to an ice–water bath and by recording the bulk solvent relaxation rate on a reference water or buffer sample.

2.3. Analysis of MRD Data. Water \(^{2}H\) and \(^{17}O\) MRD profiles, \(R_{i}(\omega_{0})\), from free-tumbling Mb in solution samples were analyzed with the standard multicomponent exchange model

\[
R_{i}(\omega_{0}) = R_{i}^{0} + \frac{1}{N_{W}}[N_{H}(\omega_{0})R_{i}^{H} - R_{i}^{0} + \sum_{k} N_{k}R_{i}^{k}(\omega_{0})]
\]

where \(\omega_{0}\) is the Larmor frequency in rad s\(^{-1}\), \(R_{i}^{0}\) is the known frequency-independence bulk solvent relaxation rate, and \(N_{W}\) is the known water/Mb molar ratio in the sample. The inverse proportionality of the excess relaxation rate, \(R_{i}^{H}(\omega_{0}) \equiv R_{i}(\omega_{0}) - R_{i}^{0}\), to \(N_{W}\) was used to normalize all MRD data to the same Mb concentration, corresponding to \(N_{W} = 3 \times 10^{14}\). In eq 1, a component \(k\), as identified by MRD profile analysis, may include several sites with similar correlation times (see below).

The first, frequency-independent, term within brackets in eq 1 refers to the external hydration shell, comprising \(N_{H}\) water molecules with average dynamic perturbation factor \(\xi_{H}\) \(\equiv \tau_{H}/\tau_{W}\). We estimate \(N_{H} = 727\) by computing the solvent-accessible surface area for equine Mb (average of PDB structures 1DWR, 1WLA, and 2VIIK) with a probe radius of 1.7 Å and dividing by the mean surface area, 10.75 Å\(^{2}\), occupied by one water molecule.\(^{67}\) The second term, \(R_{i}^{H}(\omega_{0})\), within brackets in eq 1 arises from internal water molecules (and labile deuterons), with \(N_{i}\) water molecules (or labile-deuteron water equivalents) in component \(k\) with intrinsic relaxation rate \(R_{i}^{k}(\omega_{0})\). Formally, \(N_{i}\) is the sum of occupancies of the sites belonging to component \(k\). \(N_{i}\) can be non-integer, since these sites may be partially occupied.

In MbCO, the iron is in the diamagnetic ferrous low-spin state so there is no paramagnetic contribution to the water \(^{2}H\) or \(^{17}O\) relaxation rate. The intrinsic relaxation rate, induced by the nuclear electric quadrupole coupling, is described in the model-free approach\(^{66,68}\):

\[
R_{i}^{k}(\omega_{0}) = S_{\text{iso}}^{2}O_{q}^{2}\tau_{C,k}\frac{0.2}{1 + (\omega_{0}\tau_{C,k})^{2}} + 0.8\frac{1}{1 + (2\omega_{0}\tau_{C,k})^{2}}
\]

The contribution from internal motions in the hydration site, typically on a sub-ps time scale, is negligibly small and has been omitted in eq 2. Here, \(S_{\text{iso}}\) is the usual isotropic orientational order parameter\(^{59,60,68}\) and \(\omega_{q}\) is the rigid-lattice nuclear quadrupole frequency (8.70 × 10\(^{6}\) rad s\(^{-1}\) for \(^{2}H\) and 7.61 × 10\(^{6}\) rad s\(^{-1}\) for \(^{17}O\)).\(^{59}\) The correlation time \(\tau_{C,k}\) is related to the tumbling time \(\tau_{H}\) of the protein (assumed to undergo spherical-top rotational diffusion) and the mean survival time (MST) \(\tau_{MST}\) of a water molecule in site \(k\) as\(^{60,68}\):

\[
1/\tau_{C,k} = 1/\tau_{MST} + 1/\tau_{H}
\]

Note that the survival time, often referred to as the residence time in the literature, is the time interval from an arbitrary time point to the next water exchange event.\(^{69}\)

The isotropic rank-2 rotational correlation time \(\tau_{MST}\) for Mb was obtained from molecular hydrodynamics calculations using the program\(^{70}\) HYDROPRO v. 10 with the recommended\(^{71}\) effective (non-hydrogen) atomic radius of 3.0 Å and the 1.45 Å resolution crystal structure 1DWR of equine MbCO.\(^7\) Corrected to the viscosity of D\(_{2}\)O at 25 °C, we thus obtained \(\tau_{MST} = 11.1\) ns, close to the value, 11.9 ± 0.4 ns, deduced\(^{2}\) (after correction to D\(_{2}\)O viscosity) from the field-dependent paramagnetic transverse relaxation rate of the proximal histidine H\(^{\text{65}}\) in equine deoxy-Mb at 25 °C. Because of its oblate-like shape, Mb actually undergoes anisotropic rotational diffusion, but the computed 17% span of the five asymmetric-top rotational correlation times cannot be resolved by our MRD data.

As it stands, eq 1 is strictly valid only in the fast-exchange regime, where the MST in each site \(k\) that contributes significantly to \(R_{i}(\omega_{0})\) is sufficiently short that \(R_{i}^{H}(0)/\tau_{MST} < 1\). In the dilute regime, however, eq 1 remains valid to an excellent approximation for arbitrarily long MST, provided that \(N_{i}\) and \(\tau_{C,k}\) in eqs 1 and 2 are reinterpreted as effective parameters according\(^{60,68}\):

\[
\frac{N_{i}^{\text{eff}}}{N_{i}} = \frac{\tau_{C,k}^{\text{eff}}}{\tau_{C,k}} = \left[1 + \omega_{0}^{2}S_{\text{iso}}^{2}O_{q}^{2}\tau_{C,k}\tau_{MST}\right]^{-1/2}
\]

Water \(^{2}H\) MRD profiles from immobilized Mb in gel samples were analyzed with the exchange-mediated orientational randomization (EMOR) model\(^6\) which has recently been quantitatively validated with the aid of an ultralong MD simulation of the protein BP\(_{1}\)\(^{68}\). Since the cross-linked protein cannot tumble, the water orientation is randomized by the exchange process itself, so that \(\tau_{C,k} = \tau_{MST}\). As a consequence, the conventional perturbation theory of spin relaxation is only valid in the fast-exchange regime, where \(\omega_{0}\tau_{MST} < 1\). In this regime, the EMOR theory reduces to eqs 1 and 2 (with \(\tau_{C,k} = \tau_{MST}\)). Outside this regime, meaning \(\tau_{C,k} > 1/\omega_{0}\approx 1\mu s\), the general form of the EMOR theory, based on the stochastic Liouville equation, must be used.\(^{62}\) All fits to \(^{2}H\) MRD data from immobilized MbCO reported here are based on eq 4.7 of ref 62, which is exact in the dilute regime \((N_{W} \gg 1)\). Whereas, in the solution case, each component \(k\) is modeled by the two parameters \(N_{i}^{S}S_{\text{iso}}^{2}O_{q}^{2}\) and \(\tau_{C,k}\) (or their effective counterparts), there are four parameters in the gel case: \(N_{i}^{G}, S_{\text{iso}}, \eta_{M}, \tau_{MST}\). Two of these parameters are related to the isotropic order parameter as\(^{62}\):

\[
S_{\text{iso}}^{G} = S_{\text{iso}}(1 + \eta_{M}^{2}/3)^{1/2}
\]

Since the \(^{17}O\) nuclide has spin quantum number \(I = 5/2\), the relaxation behavior is in general more complex than that for \(^{2}H\) with \(I = 1\).\(^{59,61}\) In the dilute regime, however, eqs 1–3 remain valid to an excellent approximation in the solution case.\(^{59,73}\) In the gel case, approximate expressions\(^{61}\) are available for arbitrary \(\tau_{MST}\), while for \(\tau_{C,k} < 1/\omega_{0}\approx 100\) ns the EMOR theory reduces to eqs 1 and 2, which are valid also for \(^{17}O\).\(^{59,73}\)

In fitting these models to the MRD data, we used the trust-region reflective non-linear optimization algorithm\(^74\) with uniform 0.5% \(^{17}O\) solution MRD) or 1.0% (all other MRD profiles) \(R_{0}\) error, estimated from the scatter of the frequency independent bulk relaxation rate, \(R_{i}^{0}\). With this algorithm, the model parameters can be constrained to their physically admissible ranges.
3. RESULTS AND DISCUSSION

3.1. Overview of MRD. Because $^2$H relaxation is relatively slow, the field-cycling technique$^{59,66}$ can be used to measure the MRD profile from immobilized Mb down to 1.5 kHz, allowing internal-water exchange to be monitored on time scales up to 10 μs. The drawback is that $^2$H relaxation does not probe water deuterons exclusively but also may contain a contribution from labile deuterons (LDs) in acidic protein side chains.$^{59,61,75,76}$ (This problem is even more severe for $^1$H MRD.$^{59,77,78}$) An essential step in the interpretation of $^2$H MRD data is therefore to separate the contributions from D$_2$O molecules and LDs. To do this, we use four strategies: (1) we vary pD to change the acid- and base-catalyzed LD exchange rate and to titrate the LD-bearing side chains; (2) we use different buffers to examine buffer-catalyzed LD exchange; (3) we compare $^3$H MRD profiles from immobilized Mb with profiles from solutions of free-tumbling Mb, where the LD effect is usually more pronounced; and (4) we record $^{17}$O MRD profiles (for both immobilized and free-tumbling Mb), which monitor water molecules exclusively but do not extend below 0.7 MHz.

In sections 3.2–3.4, we analyze the $^3$H and $^{17}$O MRD data. The interpretation of the data gives a consistent picture of the internal hydration of Mb but involves several technical details. As a guide to the reader, we summarize the key findings here.

$^3$H MRD profiles from immobilized MbCO show three dispersion components with characteristic mean survival times (MSTs) of 5.6 μs, 121 ns, and 6 ns, respectively. The one with the slowest MST (5.6 μs) is the dominant component and is attributed to internal water molecules and labile $^3$H in histidine side chains. The other two components are assigned to internal motions of His side chains (121 ns) and to confined external water molecules (6 ns), as seen in the previous protein gel MRD study.$^{61}$ The pD dependence of the gel $^3$H MRD profiles demonstrates that 5.2 ± 0.6 internal water molecules and two or three His side chains are responsible for the 5.6 μs component.

Solution $^3$H MRD profiles from free-tumbling MbCO can be described by a single dispersion component. This component is attributed to the two slow components (5.6 μs and 121 ns), and the obtained parameters are consistent with the gel profiles.

The $^{17}$O MRD profile from immobilized MbCO reveals an additional internal water molecule with an MST of 32 ns. This water molecule is not evident in the $^3$H MRD data, presumably because 180° flips about the water dipole axis reduce the $^3$H order parameter. The solution $^{17}$O MRD profile is described by a single component just like the solution $^3$H MRD. The solution $^{17}$O MRD can be accounted for by the 5.6 μs and 32 ns components, whereas the solution $^3$H dispersion is produced by the 5.6 μs and 121 ns components. The gel and solution $^{17}$O MRD profiles indicate that 3.9 ± 0.6 internal water molecules are responsible for the 5.6 μs component, whereas the $^3$H analysis yields 5.2 ± 0.6. Our final estimate of 4.5 ± 1.0 internal water molecules with an MST of 5.6 μs is the average of the $^3$H and $^{17}$O derived results.

3.2. $^2$H MRD from Immobilized MbCO. $^2$H MRD profiles from MbCO immobilized by cross-linking with GA, which reacts primarily with lysine side chains,$^{62}$ were recorded at different Mb concentrations, GA/Mb mole ratios (N$_{GA}$), pD values, buffer conditions, and temperatures, in all 25 profiles (Table S1, Supporting Information). Figure 2a shows a typical profile, measured at pD 7.0. The first thing to note is that the low-frequency dispersion has a large amplitude, ~3 times (after $N_w$ normalization) that obtained from the protein BPTI with three contributing internal water molecules.$^{63}$ The dominant contribution to this large dispersion is a component with an MST of 5.6 ± 0.5 μs (Figure 2a, Table 1). To reveal any LD contribution to this large dispersion, we recorded MRD profiles at different pD values in the range 5.66–7.15. pD values outside this range were excluded by heme dissociation$^{63}$ and concomitant Mb aggregation (lower pD) or by the GA cross-linking chemistry$^{64}$ (higher pD).

Figure 2b shows the pD dependence of the zero-frequency excess relaxation rate $R_1^m(0) ≡ R_1(0) − R_0$, extrapolated from the $R_1$ data with the aid of the parameters derived from fits to 22 individual MRD profiles like the one in Figure 2a (Table S1, Supporting Information). Several conclusions can be drawn from these results. Since all data points fall on the same master curve despite having been recorded on samples with different

![Figure 2](image-url)
Mb concentration (1.02–2.65 mM) and different NLD (29.7–110), we infer that the internal-water dynamics probed by the MRD profile do not depend significantly on parameters that might affect the structure of the cross-linked protein network. When the Mb concentration was raised to 5.14 mM, however, a 23% reduction of R1\(^{a}\) (0) was observed. This might be due to impaired exchange for some of the internal water molecules or labile deuterons caused by increased protein–protein contacts at high concentration. The subsequent analysis of MRD data from immobilized Mb is restricted to samples with C\(_{Mb}\) = 1.6 mM and NLD = 30.

The second major conclusion that follows from the data in Figure 2b is that R1\(^{a}\) (0) must have a significant LD contribution. Before attempting to separate the pD-dependent LD contribution from the pD-independent internal-water contribution, we shall identify the side chains and the exchange mechanism responsible for the LD contribution. In doing so, we are guided by two observational facts: (1) the LD contribution to R1\(^{a}\) (0) decreases with pD in the investigated pD range 5.66–7.15, and (2) the MST, \(\tau_{LD}\), of the LDs must be close to the 5.6 \(\mu\)s MST of the dominant dispersion component (Table 1). In the slow-exchange regime (\(\tau_{LD} > 1 \mu\)s), we expect the LD contribution to R1\(^{a}\) (0) to be approximately proportional to \(N_{LD}(pD)/\tau_{LD}(pD)\).\(^{62}\) The observed pD dependence can hence reflect changes in the number, \(N_{LD}\), of LDs and/or in \(\tau_{LD}\).

The LD exchange mechanism can be intermolecular (involving a single side chain and one or more solvent species including buffer ions) or intramolecular (involving two proximal side chains). We consider first the usual intermolecular mechanism. Due to the observed buffer independence of R1\(^{a}\) (0) (Figure 2b), buffer catalyzed LD exchange can be neglected. We therefore need to consider only the acid (D2O\(^+\)) and base (OD\(^–\)) catalyzed exchange mechanisms. LD exchange from basic groups (Arg, Lys, His, N-terminus) is base catalyzed in the examined pD range. Any LD contribution from these groups would vary with pD as \(N_{LD}/\tau_{LD} \propto 1/(10^{-pK_{a}} + 10^{-pD})\); that is, it would increase monotonically with pD, in contrast to the observed decrease (Figure 2b). Furthermore, even if base catalyzed LD exchange proceeds at the maximum (diffusion controlled) rate, \(\tau_{LD}\) at pD 7 is 3 orders of magnitude longer than the required \(\mu\)s time scale. LD exchange from hydroxyl-bearing groups (Ser, Thr, Tyr) is both acid and base catalyzed. In principle, the observed pD dependence (Figure 2b) could therefore reflect acid catalysis. The rate constant, \(k_{a}\), for acid catalysis is, however, typically 4 orders of magnitude smaller than the rate constant, \(k_{b}\), for base catalysis.\(^{75,76,79}\) The minimum LD exchange rate should therefore occur close to pD = (1/2) log\([k_{a}/(K_{W}k_{b})]\) \(\approx 5.5\), where \(K_{W} = 10^{-14.5}\). In the examined pD range, we would therefore expect R1\(^{a}\) (0) to increase with pD if hydroxyl LDs were responsible. Furthermore, even with the maximum conceivable rate constants\(^{75,76,79}\) (\(k_{a} \approx 10^{-9} \text{ M}^{-1} \text{s}^{-1}\) and \(k_{b} \approx 10^{-11} \text{ M}^{-1} \text{s}^{-1}\)), \(\tau_{LD}\) is too long, by at least 2 orders of magnitude, in the examined pD range. LD exchange from carbonyl groups (Asp, Glu, C-terminus) usually occurs directly to water without involvement of catalytic species, so that \(\tau_{LD}\) is independent of pD.\(^{75,76}\) In principle, the observed pD dependence (Figure 2b) could therefore reflect deprotonation of COOD groups. For immobilized BPTI, a small COOD contribution was seen at pD 4.4, but not at pD 6.5 where all carbonyl groups in BPTI are deprotonated.\(^{61}\) For MbCO, carbonyl groups with strongly upshifted pKa values are not indicated,\(^{80}\) so carbonyl LDs cannot explain the pD dependence in Figure 2b.

On the basis of these considerations, we conclude that the LD contribution observed here is produced by intramolecular LD exchange with an essentially pD-independent rate. The observed pD dependence in R1\(^{a}\) (0) must then reflect the ionization equilibrium. With no pKa upshifted carbonyl group, only the imidazolium (His) groups are titrated in the examined pD range. Equine Mb contains 11 histidines (BPTI has none) and different exchange mechanisms for His LDs can be found in section S1 (Supporting Information).\(^{83}\) We then expect that R1\(^{a}\) (0) \(\approx a + N_{LD}(pD)b\), where \(a\) is the internal water contribution and \(N_{LD}\) is the number of labile His deuterons (two in the acidic form, none in the basic form). Using published pKa values\(^{80–83}\) we find that this function can reproduce the observed pD dependence in R1\(^{a}\) (0). The fit shown in Figure 2b yields a pD-independent contribution (the parameter \(a\)) to R1\(^{a}\) (0) of 26.4 s\(^{-1}\), corresponding to 73.1% of R1\(^{a}\) (0) at pD 7.0. Although all the His residues were included in this analysis, the result only depends on the pKa distribution (in the examined pD range) and not on the number of His residues. Indeed, very similar results are obtained (26.2 s\(^{-1}\) and 73.3%) if we assume that the pD dependence is produced by a single His residue with a typical pKa value of 6.5.

The LDs of His side chains can exchange via an intramolecular exchange mechanism, where a water molecule bridges a positive His residue and negative carboxylic acid group or a positive/negative His pair (section S1, Supporting Information), similar to what has been proposed for certain low-molecular-weight His derivatives.\(^{84}\) The crystal structure of equine MbCO reveals several His residues that could engage in such intramolecular exchange (section S1, Supporting Information). A more detailed discussion of different exchange mechanisms for His LDs can be found in section S1 (Supporting Information).

The 2H MRD profiles from immobilized MbCO are strongly dominated by the slowest kinetic component (Figure 2a), hereafter referred to as component 1. At pD 7.0, the fit yields \(N_{1} = 6.7 \pm 0.8\) for the number of water molecules and/or LD water equivalents (one acidic His residue equates to one D2O molecule) responsible for this component (Table 1). Hydration sites may have fractional occupancy and His residues may be partly titrated, so \(N_{1}\) need not be an integer. The analysis in

**Table 1. Results of Fits to 2H and 17O MRD Profiles**

| \(\nu^p\) parameter | \(2H\) | \(17O\) | \(2H\) | \(17O\) |
|----------------------|-------|-------|-------|-------|
| \(\tau_{LD}(\mu s)\) | \(5.6 \pm 0.5\) | [5.6] | \(6.7 \pm 0.8\) | \[5.2\] |
| \(N_{1}\) | \(0.79 \pm 0.02\) | \[0.79\] | \(0.3 \pm 0.1\) | \[0\] |
| \(S_{1}\) | \(6.7 \pm 0.8\) | \[5.2\] | \(6.7 \pm 0.8\) | \[5.2\] |
| \(N_{k}\) | \(0.79 \pm 0.03\) | \[0.79\] | \(6.7 \pm 0.8\) | \[5.2\] |
| \(\xi_{1}\) | \(6.7 \pm 0.8\) | \[5.2\] | \(6.7 \pm 0.8\) | \[5.2\] |
| \(\lambda_{1}\) | \(6.7 \pm 0.8\) | \[5.2\] | \(6.7 \pm 0.8\) | \[5.2\] |
| \(\lambda_{2}\) | \(6.7 \pm 0.8\) | \[5.2\] | \(6.7 \pm 0.8\) | \[5.2\] |

\(^{a}\)All four MRD profiles were measured at 25 °C and pD 7.0. Quoted errors correspond to one standard deviation, propagated from the uniform 0.5 or 1.0% uncertainty in \(R_{1}\). Parameter values within square brackets were fixed during the fit. \(^{b}\)Component 2 has different physical origins in the four cases (see text).
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Figure 2b indicates that 73.1% of $R_i^N(0)$ is produced by water deuterons at pD 7.0 and the MRD fit in Figure 2a shows that $R_i^N(0)$ at pD 7.0 can be broken down as follows: 91.3% component 1 (with contributions from water and LDs), 6.1% component 2 (entirely due to LDs; see below), and 2.6% from component 3 and the frequency-independent hydration-shell component (both entirely due to water; see below). We thus infer that $(73.1 - 2.6)/0.913 = 77.2\%$ of component 1 is produced by $N_i^W = 0.772N_i = 5.2 \pm 0.6$ internal water molecules.

The remaining 22.8% of component 1 at pD 7.0 is attributed to LDs in His residues (see above). If the locally averaged nuclear quadrupole coupling is the same for the LDs as for the ~5 internal water molecules, we can infer that $N_i^{LD} = 3.0 \pm 0.4$ LDs contribute to component 1 at pD 7.0. Since (the rigid-lattice) $^2$H quadrupole coupling constant for the acidic imidazole deuterons is expected to be smaller than for $D_2O$, the actual value of $N_i^{LD}$ may be as large as five. We therefore conclude that at least two, and possibly three, His side chains (with two LDs per imidazolium group) engage in water-mediated intramolecular LD exchange on the $\mu$s time scale.

According to the fit, the MST of the water molecules contributing to component 1 is $r_{S,1} = 5.6 \pm 0.5 \mu s$ (Table 1). That ~5 internal water molecules, located at different sites within the MbCO molecule, have the same MST suggests that they exchange by a common mechanism (section 3.6). But it should be noted that even though the dominant low-frequency dispersion is reproduced by a single kinetic EMOR component, a modest MST distribution would not have been resolved by our data.

The value $r_{S,1} = 5.6 \mu s$ is on the long side of the maximum of $R_i(t)$ versus $t$ corresponding to $r_{S} \approx 1/\omega_Q \approx 1 \mu s$. In this slow-exchange regime, $R_i(0)$ decreases with increasing $r_S$. For example, if $r_{S,1}$ had been 1 $\mu s$, $R_i(0)$ would have been several-fold larger and the dispersion would have appeared at a higher frequency. If $r_{S,1}$ had been much longer, say 50 $\mu s$, then the dispersion frequency would only have been slightly down-shifted, but the amplitude would have been strongly reduced.

In other words, a much larger number of internal water molecules or LDs would have been required to account for the observed MRD profile if the MST were much longer. In fact, in the ultrasonic motion regime, where $r_S \gg 1/\omega_Q \approx 1 \mu s$, $R_i(0)$ is approximately proportional to $N_i/r_S^2$. Even though the observed 5.6 $\mu s$ MST is not long enough to be in this regime, the parameters $N_i$ and $r_{S,1}$ have a sizable covariance. Reassuringly, constrained fits to the $^2$H MRD profile with different fixed values of $N_i$ yield the best fit quality for $N_i$ between six and seven (Figure S2, Supporting Information), consistent with the result, $N_i = 6.7 \pm 0.8$, from the unconstrained fit.

To reproduce the $^2$H MRD profile also at higher frequencies, the model must include, in addition to the dominant 5 $\mu s$ component, two components in the fast-exchange regime (Table 1). One of these components has $r_{S,2} = 0.12 \pm 0.01 \mu s$ and $N_i^{S,2} = 0.70 \pm 0.03$. As argued in section 3.4, this component can be attributed to internal motions of rapidly exchanging LDs in His side chains. The third dispersion component has $r_{S,3} = 6 \pm 1 \mu s$ and $N_i^{S,3} = 3.6 \pm 0.6$ (Table 1). Similar parameter values were obtained for the highest-frequency component of the $^2$H MRD profiles of immobilized BPTI and ubiquitin. As before, we attribute this component to a small number of confined water molecules in the external hydration shell. Finally, the dynamic perturbation factor, $\xi_H = 7.3 \pm 0.5$, deduced from the frequency-independent excess relaxation, is somewhat larger than that for free-tumbling Mb (section 3.3).

In summary, the high-frequency tail of the $^2$H MRD profile from immobilized MbCO exhibits the expected features associated with the external hydration shell, whereas the low-frequency part (components 1 and 2) reflects the occupancy and dynamics of internal hydration sites and LDs in a few His residues. The observed pD dependence of the $^2$H MRD profile indicates that 5.2 $\pm 0.6$ internal water molecules with MST 5.6 $\pm 0.5 \mu s$ contribute to the dominant dispersion component.

3.3. $^2$H MRD from Free-Tumbling MbCO. As a check on the interpretation of the $^2$H MRD data from immobilized MbCO, we measured the $^2$H MRD profile from free-tumbling MbCO in solutions with pD in the range 5.0–10.0. (For the gel samples, the cross-linking chemistry limited us to pD $\leq 7.2$.) In the acidic pD range, a low-frequency MRD component was observed with a correlation time corresponding to tumbling of large protein aggregates, presumably induced by heme dissociation.

At pD 5.0, this component dominated the $^2$H MRD profile. We therefore restrict the analysis to $R_i$ data measured at $\omega_0/2\pi > 0.9$ MHz on solutions with pD $\geq 6$. Under these conditions, the fraction aggregated protein is so small (<1%) that the associated $R_i$ contribution can be neglected.

Figure 3a shows the $^2$H MRD profile from free-tumbling MbCO at pD 7.0. At all pD values in the range 6.0–10.0, the MRD data (for $\omega_0/2\pi > 0.9$ MHz) can be adequately represented by a single dispersion component. The correlation time, $\tau_C$, deduced from the single-component fit is shorter than the Mb tumbling time, $\tau_S = 11.1$ ns (section 2.3) and it decreases with increasing pD: from 9.6 $\pm 0.4$ ns at pD 6.0 to 7.4 $\pm 0.5$ ns at pD 10.0 (Figure 3b). These findings can be explained if there is a pD-dependent contribution from LDs exchanging on the ~100 $\mu$s time scale, as expected for base-catalyzed LD exchange in hydroxyl, ammonium, and guanidinium groups. In contrast to the rapidly exchanging His LDs (section 3.2), these more slowly exchanging LDs do not contribute to the $^2$H MRD profile from immobilized MbCO because of the more restrictive fast-exchange criterion $\omega_0/2\pi < 1$. For a free-tumbling protein, the fast-exchange criterion is $\omega_0(S\tau_S)^{1/2} < 1$ (section 2.3), so LDs with $\tau_S$ on the order of 100 $\mu$s make a significant contribution, albeit with reduced effective weight $N_S^{eff}$ and correlation time $\tau_C^{eff}$ according to eq 3. As explained in more detail in section S2, $\tau_C$ decreases with pD (Figure 3b) because the relative contribution to the MRD profile from LDs with reduced effective correlation time increases with pD.

The pD dependence of the amplitude parameter $N_S^{iso}$ has a broad minimum of 5.0 $\pm 0.3$ at pD 8–9 (Figure 3b). It decreases first because the His residues involved in intramolecular LD exchange are titrated (section 3.2), consistent with the decrease of $R_i^N(0)$ with pD in Figure 2b. Above pD ~9, where all His residues in equine Mb are titrated, increases because base-catalyzed exchange brings an increasing...
This value is within the range found for other proteins. At 5.6 ± 6.0 frequency-independent pD 10, pro 3a) must include both components 1 and 2 in the gel MRD. Motions of rapidly exchanging LDs. NS slightly differs in Mb into the fast-exchange regime. The number of hydroxyl-bearing or basic (mainly Arg) side chains contribute very little to the 17O MRD profile from immobilized MbCO. Nevertheless, the 17O MRD profile from immobilized MbCO at pD 7.0 exhibits a large dispersion in the examined frequency range (Figure 4a). In analyzing this MRD profile, we include the small contribution from component 1, taking τH,1 = 5.6 μs and S1 = 0.79 from the 2H MRD fit (Table 1) and using the estimate N1 = 5.2 for the number of water molecules associated with this component (section 3.2). Even at the lowest frequency, this contribution hardly exceeds the measurement error in R1 (Figure 4a). Beyond this minor contribution, two fast-exchange components are required to account for the 17O MRD profile (Table 1).

The dynamic perturbation factor χH and the parameters τH,3 and N3S3H of the fastest dispersion component do not differ significantly from the corresponding 2H parameters (Table 1), as expected if these contributions reflect weakly anisotropic water motions in the external hydration shell in the gel. The amplitude parameter, N3S3H = 1.0 ± 0.1, of the slower 17O component is similar to that of 2H component 2 (Table 1), but the factor 4 difference in the associated correlation times shows that these components have different physical origins. A water molecule with 120 ns MST would give rise to a very large 17O dispersion, which is not observed, so we must conclude that this 2H component is produced by LDs. Since 120 ns is too short to be an MST for a LD (all carboxyl groups are titrated at pD 7.0), we assign 2H component 2 to internal motions of the His residues that contribute to 2H component 1. Internal motions of protein side chains on this time scale have previously been inferred from 2H MRD studies of several proteins. 17O component 2, on the other hand, must reflect water motions. In principle, this could be local motions of the 5 μs internal waters. The only local water motion that might be as slow as 32 ns, however, is a 180° flip about the dipole axis, which, for symmetry reasons, cannot induce 17O relaxation. We therefore conclude that the dominant 17O component 2 represents a single highly ordered water molecule with an MST of 32 ± 3 ns. This water molecule is unlikely to be deeply buried, and it must exchange by a different mechanism that than used by the 5 μs waters. But why is this water molecule not evident as a 32 ns component in the 2H profile? If it undergoes 180° flips on the time scale 0.1−10 μs, the 2H parameter S1H is reduced by a factor of 3. The contribution of this water molecule would then not be resolved because it would only add

![Figure 3](image-url)
A quantitative analysis of the two contributions to $N_{\text{iso}}^{\mu}$, which is proportional to the magnitude of the dispersion, shows that the solution and gel $^{17}$O MRD profiles are consistent, within the experimental error, with the gel $^2$H MRD profile (section S3, Figure S4, Supporting Information). Of particular interest is the number $N_{\text{iso}}^{\mu}$ of internal water molecules with an MST of 5.6 μs. Our analysis of the pD dependence of the gel MRD profile (section 3.2) indicates that $N_{\text{iso}}^{\mu} = 5.2$, but the $^{17}$O MRD data suggest a somewhat smaller value (section S3, Figure S4, Supporting Information). Averaging these results, we arrive at the conservative estimate $N_{\text{iso}}^{\mu} = 4.5 \pm 1.0$.

In summary, all the $^2$H and $^{17}$O MRD profiles measured on MbCO gels and solutions can be interpreted in a self-consistent way. The gel $^2$H MRD profile and the solution $^{17}$O MRD profile are both consistent with $N_{\text{iso}}^{\mu} = 4.5 \pm 1.0$ ordered water molecules with an MST of 5.6 ± 0.5 μs. The solution and gel $^{17}$O MRD profiles indicate an additional component, not resolved in the $^2$H profiles, comprising a single highly ordered water molecule with an MST of 32 ± 3 ns.

### 3.5. Internal Hydration Sites

MRD experiments can provide the number of internal water molecules and their mean survival times, but the location of a hydration site can only be determined by MRD if the water molecule can be displaced by a ligand or a substituted side chain. Mb contains four cavities, denoted Xe1–Xe4 (Figure 1), that have been shown to bind xenon at elevated pressure. To determine if the internal water molecules identified here occupy any of the Xe sites, we recorded the $^2$H MRD profile from an MbCO gel that had been equilibrated with 8 bar of Xe gas. We determined the Xe occupancies of these sites from $^{129}$Xe NMR spectra of the MbCO gel and of two reference samples (Figure S5, Supporting Information), using also the reported $^{129}$Xe binding constants for equine Mb at pH 7.0 and 25°C. In this way, we obtained a Xe occupancy of 0.80 ± 0.09 for site Xe1 and a combined occupancy of 0.10 ± 0.05 for sites Xe2–Xe4 (section S4, Tables S3 and S4, Supporting Information).

As seen from Figure 5 and Table S5 (Supporting Information), Xe binding at this level has no significant effect on the $^2$H MRD profile. With 80% Xe occupancy in Xe1, we would have expected 100 × 0.8/6.3 = 13% reduction of $R_t$ at a small dispersion amplitude (0.3 s⁻¹ in $R_t$) between the 6 and 121 ns dispersion steps (Figure 2a).

As in the $^2$H case, the $^{17}$O MRD profile from free-tumbling MbCO is well described by a single dispersion component (Figure 4b). The dynamic perturbation factor, $\xi = 5.8 \pm 0.1$, is the same as that obtained from the $^2$H solution profile (Table 1), as expected since water motions in the external hydration shell are nearly isotropic. The correlation time, $\tau_c = 5.6 \pm 0.2$ ns, is shorter than the Mb tumbling time, $\tau_T = 11.1$ ns, because the single $^{17}$O solution MRD component is an unresolved superposition of two components, both with correlation times shorter than $\tau_T$. The first component, due to water molecules with $\tau_s = 5.6$ μs as deduced from the gel $^2$H MRD profile, is in the intermediate-exchange regime for $^{17}$O, with the effective correlation time shortened by a factor of ~2 according to eq 3. The contribution of this component to the total amplitude parameter, $N_{\text{iso}}^{\mu} = 3.0 \pm 0.1$ (Table 1), is reduced by the same factor. The second component, due to the single water molecule with $\tau_s = 32$ ns as deduced from the gel $^{17}$O MRD profile, is in the fast-exchange regime with effective correlation time $(1/\tau_0 + 1/\tau_s)^{-1} = 8.3 \pm 0.2$ ns (section 2.3).

![Image](attachment:image.png)
low frequency if Xe1 had been fully occupied by a long-lived water molecule. We can therefore rule out internal water in this site. This is hardly surprising, since Xe1 has by far the highest Xe affinity among the four Xe sites and thus is expected to be the least polar site. For the other sites, the combined 10 ± 5% Xe occupancy is probably not sufficient to produce a detectable reduction of the MRD amplitude even if all these sites were fully occupied by water in the absence of Xe. If one Xe atom displaces one water molecule, MRD component 1 would be reduced by merely 1.5% (0.1/6.7), comparable to the measurement error.

All high-resolution crystal structures of equine and sperm whale Mb, in the CO, deoxy, or met forms, identify two internal hydration sites in the Xe3 cavity, with full (equine Mb) or nearly full (sperm whale Mb) occupancy (Figures 1 and S6, Tables S6 and S7, Supporting Information). The water molecule in subsite Xe3a has a small B factor and is engaged in four H-bonds, donating to Ile-75 O and His-82 N and accepting from Gly-80 N and the adjacent water molecule. The water molecule in subsite Xe3b has a much larger B factor and makes only one H-bond with the protein (Ala-134 O). In addition, all but one of the high-resolution crystal structures listed in Tables S6 and S7 (Supporting Information) locate an internal water molecule in the so-called apical site (Figures 1 and S6, Tables S6 and S7, Supporting Information). The apical water makes three H-bonds with the protein. The crystal structures of equine Mb (but not sperm whale Mb) in the CO and deoxy (but not met) forms also locate a water molecule in the “bottom” site (Figures 1 and S6, Tables S6 and S7, Supporting Information). The bottom water also makes three H-bonds with the protein, but it is less deeply buried than the apical water.

It is tempting to identify these four crystallographic water molecules with the 4.5 ± 1.0 most long-lived (5 μs) water molecules indicated by the MRD data. The Xe difference MRD experiment does not rule out the presence of two water molecules in the Xe3 cavity because Xe appears to displace only one of these water molecules (at least for sperm whale Mb; see PDB entries 1J52 and 2W6Y), and then, as noted above, the effect would be too small to detect. Furthermore, the 10 ± 5% combined Xe occupancy is presumably associated mainly with the less polar Xe2 and Xe4 cavities. The 32 ns water inferred from the 1H MRD data might be located in a deep surface pocket. Alternatively, it could refer to one of the two least deeply buried among the four internal hydration sites, the bottom site and subsite Xe3b. In that case, another internal hydration site, not identified in the crystal structures, must contribute to the 5 μs MRD component. For example, the phantom (Ph) cavity (Figure 1) is large enough to accommodate four (mutually H-bonded) water molecules, but this cavity is empty in all the crystal structures of equine Mb.

The two MD simulation studies that have focused on internal water in Mb both find multiple partially occupied hydration sites most of which have not been identified in crystal structures. The first of these studies, a conventional MD simulation of equine met-Mb at 300 K, found, in addition to the Fe-bound water in the DP, eight internal hydration sites with a combined occupancy of 2.75. The apical site (occupancy 0.8) was identified but not the bottom site. Both the Xe3 and Xe4 cavities were assigned an occupancy of 0.3. Except for the iron-bound water, all internal water molecules identified from this 48 ns MD trajectory exchanged on a nanosecond timescale. Therefore, this MD study supports neither the crystallographically inferred locations and occupancies of internal hydration sites in Mb nor the MRD-inferred microsecond timescale of internal water exchange.

The second simulation study examined sperm whale deoxy-Mb at 310 K and used temperature-accelerated MD for enhanced sampling. Numerous internal hydration sites (but no occupancies) were reported, including the Xe2, Xe3, and Xe4 (but not Xe1) cavities. On the basis of computed minimum free energy pathways for water migration, it was suggested that all internal water molecules enter the protein via the His-64 gate and the DP, from where water molecules can migrate further to the Xe cavities. With the aid of transition state theory, the time scale for water escape from the DP was estimated at 300 ns (at 310 K), an order of magnitude faster than the 5 μs MRD deduced from our MRD data.

In summary, crystallography supports a scenario where most or all of the ~4 long-lived internal water molecules inferred by MRD reside in small polar cavities (Xe3, apical, and bottom sites). A larger number of partially occupied sites, as suggested by MD simulations, is not likely to account for the MRD data. X-ray crystallography may miss hydration sites with low occupancy and/or positional disorder, but water molecules in less polar sites (say, with less than three H-bonds) are expected to have a small order parameter and would then not contribute much to the MRD profile.

3.6. Mechanism of Internal-Water Exchange. The common MST, τS = 5.6 ± 0.5 μs, of the ~4 water internal molecules inferred from our MRD data suggests that they exchange with external solvent via a common mechanism. Moreover, since the likely internal hydration sites are located far apart in the Mb molecule (the apical, bottom, and Xe3 sites are separated by 17, 27, and 31 Å), the common exchange mechanism must be global in spatial extent.

In an effort to gain more insight into the exchange mechanism, we studied the temperature dependence of the 2H MRD profile from immobilized MbCO. Irreversible changes in the MRD profile, possibly caused by gel restructuring, were noted above 35 °C. Therefore, the analysis was restricted to the rather narrow temperature range 5–25 °C, where fits like the one in Figure 2a yielded a surprisingly small Arrhenius activation energy of 17.4 ± 0.4 kJ mol−1 for the MST τS at pD 7.0 (Figure S7, Supporting Information). Such a small activation energy might suggest that water exchange is rate-limited by an entropic bottleneck. The narrow temperature range and the strong covariance between N1 and τS (section 3.2), however, preclude an unambiguous interpretation of the temperature dependence. The MSTs used for the Arrhenius fit in Figure S7 (Supporting Information) were obtained from constrained fits where τS was the only adjustable parameter for component 1 even though the relative contributions of internal water and LDs to component 1 are expected to vary with temperature.

The ~5 μs MST deduced from our MRD analysis implies that internal-water exchange in Mb is a rare event that has not yet been captured by MD simulations, which so far do not extend beyond 100 ns for Mb. Neither the average protein structure seen in crystal structures nor the fluctuations accessed by sub-μs simulations tell us much about the transient structures involved in the water exchange event. An ultralong MD simulation was recently used to demonstrate that the internal water molecules in the protein BPTI exchange by a transient aqueduct mechanism, where single-file water chains...
penetrate the protein through transiently formed tunnels or pores. It is conceivable that a similar mechanism operates in Mb, with the difference that the transient water-filled tunnels are partly built from preexisting cavities. Whereas a single water molecule is unlikely to migrate from a polar site into a largely non-polar cavity network, an H-bonded water chain can move rapidly through a transiently formed tunnel. The peripherally located internal hydration sites might then act both as portals for solvent penetration and as seeds for transient water chains.

MD simulations indicate that the ligands can migrate from the DP into the extensive network of permanent and transient cavities that permeates the Mb molecule. The ligand migration pathways seen in these simulations include the apical and Xe3 hydration sites. A transient aqueduct mechanism might act to intermittently “flush” the cavity network, thereby removing internally trapped ligands. Experiments indicate that photodissociated CO can escape from the DP via the His-64 gate on a 100 ns time scale. The half-life of CO that has migrated from the DP to the Xe1 cavity was, however, reported to be ~10 μs (at 20 °C). Since this process occurs on the same time scale as internal-water exchange, it may, in fact, be concomitant with the proposed “flushing” of the cavity system by transient water chains.

4. CONCLUSIONS

On the basis of ²H and ¹⁷O MRD measurements on gel and solution samples, we have arrived at the following answers to the first three of the five questions posed in section 1:

1. Under physiological conditions, equine MbCO contains 4.5 ± 1.0 internal water molecules that exchange on a μs time scale. The root-mean-square orientational order parameter of these water molecules is 0.8. Another ordered water molecule, possibly located in a deep surface pocket, exchanges on a time scale of 30 ns.

2. The likely locations of the ~4 long-lived water molecules are the crystallographically identified Xe3, apical, and bottom hydration sites. In agreement with crystallography and MD simulations, the MRD results indicate that the Xe1 cavity is devoid of water.

3. Despite being located as much as 30 Å apart, the ~4 long-lived internal water molecules have the same (or very similar) MST, τ₂ = 5.6 ± 0.5 μs.

In addition, the MRD results indicate that 2 or 3 of the 11 His residues of equine Mb undergo intramolecular hydrogen exchange on a μs time scale. As regards the last two questions in the Introduction, we speculate the following:

4. The internal water molecules exchange by a global mechanism, that may involve penetration of the protein by transient H-bonded water chains, entering the protein at the peripherally located permanent hydration sites.

5. The proposed water exchange mechanism suggests a functional role, where intermittent “flushing” of the cavity system removes trapped ligands.

 ASSOCIATED CONTENT

Supporting Information

Experimental conditions for 33 MbCO samples investigated by ²H or ¹⁷O MRD (Table S1); pKₐ values for titrating His residues in equine Mb (Table S2); estimates of His LD exchange kinetics (section S1); structural basis of internal LD exchange involving His side chains in Mb (Figure S1); qualitative explanation of pD dependence of the effective correlation time deduced from solution ¹H MRD profiles (section S2); fit quality statistics for constrained fits to gel ²H MRD profile with different fixed Nₜ values (Figure S2); solution amplitude parameter N°, predicted from constrained fits to gel ²H MRD profiles (Figure S3); demonstration of the mutual consistency of ²H and ¹⁷O MRD results (section S3 and Figure S4); determination of xenon binding to MbCO by ¹²⁹Xe NMR (section S4, Figure S5, Tables S3 and S4); results of ²H gel MRD fits with and without xenon (Table S5); internal water molecules in crystal structures of equine and sperm whale MbCO (Figure S6, Tables S6 and S7); Arrhenius plot of the MST for gel ²H MRD component 1 (Figure S7). This material is available free of charge via the Internet at http://pubs.acs.org.

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Notes

The authors declare no competing financial interest.

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Supporting Information

for

Internal Water and Microsecond Dynamics in
Myoglobin

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Sweden
Table S1. Samples for MRD Experiments.

| #  | $C_{\text{Mb}}$ | type | $N_{\text{GA}}$ | pD | buffer | nuclide | range (MHz) | $n^d$ |
|----|----------------|------|-----------------|----|--------|----------|-------------|------|
| 1  | 1.98           | S    | 5.06            |    |         | $^2\text{H}$ | 0.00152 – 92.1 | 34   |
| 2  | 2.43           | S    | 6.00            |    |         | $^2\text{H}$ | 0.00152 – 92.1 | 34   |
| 3  | 2.35           | S    | 7.00            |    |         | $^2\text{H}$ | 0.00152 – 92.1 | 34   |
| 4  | 2.38           | S    | 8.03            |    |         | $^2\text{H}$ | 0.00152 – 92.1 | 34   |
| 5  | 2.28           | S    | 9.18            |    |         | $^2\text{H}$ | 0.00152 – 92.1 | 34   |
| 6  | 2.22           | S    | 9.97            |    |         | $^2\text{H}$ | 0.00152 – 92.1 | 34   |
| 7  | 1.02           | G    | 110             | 5.95 | 5 mM NaPi | $^2\text{H}$ | 0.00152 – 5.37 | 40   |
| 8  | 1.63           | G    | 62.1            | 5.66 | 5 mM NaPi | $^2\text{H}$ | 0.00152 – 5.37 | 40   |
| 9  | 1.67           | G    | 31.1            | 5.73 | 5 mM NaPi | $^2\text{H}$ | 0.00152 – 5.37 | 40   |
| 10 | 5.14           | G    | 30.5            | 5.79 | 5 mM NaPi | $^2\text{H}$ | 0.00152 – 5.37 | 40   |
| 11 | 1.35           | G    | 30.5            | 6.03 | 5 mM NaPi | $^2\text{H}$ | 0.00152 – 5.37 | 40   |
| 12 | 2.65           | G    | 30.4            | 5.90 | 5 mM NaPi | $^2\text{H}$ | 0.00152 – 5.37 | 40   |
| 13 | 1.62           | G    | 30.3            | 6.41 | 50 mM NaPi | $^2\text{H}$ | 0.00152 – 5.37 | 40   |
| 14 | 1.61           | G    | 30.5            | 6.23 | 5 mM NaPi | $^2\text{H}$ | 0.00152 – 5.37 | 40   |
| 15 | 1.61           | G    | 30.4            | 6.39 | 50 mM NaPi | $^2\text{H}$ | 0.00152 – 5.37 | 40   |
| 16 | 1.60           | G    | 30.6            | 6.70 | 50 mM NaPi | $^2\text{H}$ | 0.00152 – 5.37 | 40   |
| 17 | 1.60           | G    | 30.6            | 6.92 | 50 mM NaPi | $^2\text{H}$ | 0.00152 – 5.37 | 40   |
| 18 | 1.60           | G    | 30.6            | 6.87 | 50 mM NaPi | $^2\text{H}$ | 0.00152 – 5.37 | 40   |
| 19 | 1.61           | G    | 30.4            | 6.09 | 50 mM NaPi | $^2\text{H}$ | 0.00152 – 5.37 | 40   |
| 20 | 1.61           | G    | 30.4            | 6.75 | 50 mM MES | $^2\text{H}$ | 0.00152 – 92.1 | 45   |
| 21 | 1.61           | G    | 30.4            | 6.13 | 50 mM NaPi | $^2\text{H}$ | 0.00152 – 5.37 | 40   |
| 22 | 1.65           | G    | 29.7            | 6.12 | 50 mM MES | $^2\text{H}$ | 0.00152 – 5.37 | 40   |
| 23 | 1.64           | G    | 29.9            | 5.99 | 50 mM MES | $^2\text{H}$ | 0.00152 – 5.37 | 40   |
| 24 | 1.65           | G    | 29.8            | 6.35 | 50 mM MES | $^2\text{H}$ | 0.00152 – 5.37 | 40   |
| 25 | 1.65           | G    | 29.8            | 6.64 | 50 mM MES | $^2\text{H}$ | 0.00152 – 5.37 | 40   |
| 26 | 1.61           | G    | 30.4            | 6.75 | 50 mM MES | $^2\text{H}$ | 0.00152 – 92.1 | 45   |
| 27 | 1.62           | G    | 29.9            | 6.98 | 50 mM PIPES | $^2\text{H}$ | 0.00152 – 5.37 | 40   |
| 28 | 1.62           | G    | 29.9            | 6.95 | 50 mM PIPES | $^2\text{H}$ | 0.00152 – 5.37 | 40   |
| 29 | 1.62           | G    | 29.9            | 7.00 | 50 mM PIPES | $^2\text{H}$ | 0.00152 – 92.1 | 45   |
| 30 | 1.62           | G    | 29.9            | 7.17 | 50 mM PIPES | $^2\text{H}$ | 0.00152 – 92.1 | 46   |
| 31 | 1.62           | G    | 29.9            | 7.17 | 50 mM PIPES | $^2\text{H}$ | 0.00152 – 92.1 | 46   |
| 32 | 2.57           | S    | 7.03            |    |         | $^{17}\text{O}$ | 1.21 – 81.3 | 12   |
| 33 | 1.62           | G    | 29.9            | 7.02 | 50 mM PIPES | $^{17}\text{O}$ | 0.692 – 81.3 | 14   |

$^a$ MbCO concentration in mM.  
$^b$ Solution (S) or gel (G).  
$^c$ NaPi = sodium phosphate.  
$^d$ Number of data points.  
$^e$ Measured at 5, 15, and 25 °C.  
$^f$ In presence of 8 bar Xe.
Table S2. pKₐ* Values for Titrating His Residues in Horse Mb.¹

| residue | pKₐ* 299.5 K, 0.2 mM NaCl¹ | pKₐ* 298 K, 20 mM NaCl² | pKₐ* 298 K, 0.2 mM NaCl² |
|---------|--------------------------|---------------------|---------------------|
| 36      | 7.75 ± 0.05              | 7.67 ± 0.01         | 7.80 ± 0.02         |
| 48      | 5.50 ± 0.07              | 5.42 ± 0.02         | 5.62 ± 0.01         |
| 81      | 6.86 ± 0.05              | 6.65 ± 0.01         | 6.94 ± 0.01         |
| 113     | 5.76 ± 0.07              | 5.51 ± 0.02         | 5.87 ± 0.02         |
| 116     | 6.72 ± 0.05              | 6.66 ± 0.02         | 6.79 ± 0.01         |
| 119     | 6.51 ± 0.05              | 6.38 ± 0.02         | 6.56 ± 0.01         |

¹ The number of labile His deuterons was calculated as \( N_{LD} = 2 \sum_i [1 + 10^{pH^* - pK_{a,i}^*}]^{-1} \), where pH* and pKₐ,i* are both measured in D₂O and neither are corrected for the H/D isotope effect (which largely cancels out in the difference). The set of six pKₐ* values used for the calculation in Sec. S1 were measured at 298 K in 20 mM NaCl. In addition, we used pKₐ* = 5.91 for His-97, determined for sperm whale MbCO.² The remaining four His residues are all in the basic form in the neutral pD range of interest here.³⁴
S1. Histidine Labile-Deuteron Exchange Kinetics

We estimate the mean survival time, $\tau_{LD}$, of the acidic imidazolium deuterons from

$$\tau_{LD} = \frac{1}{k_w[D_2O] + k_b[OD^-] + k_c[Buf^-]}$$  \hspace{1cm} (S1)$$

where the three rate constants refer to the water, hydroxide, and buffer catalyzed exchange processes:

$$\geq ND^+ + D_2O \xrightarrow{k_w} \geq N: + D_3O^+$$
$$\geq ND^+ + OD^- \xrightarrow{k_b} \geq N: + D_2O$$
$$\geq ND^+ + Buf^- \xrightarrow{k_c} \geq N: + BufD$$.

Assuming that association and dissociation are diffusion-controlled with the rate constant $k_D$, the three LD exchange rate constants can be expressed as

$$k = \frac{k_D}{1 + 10^{pK_a(\text{His})-pK_a(\text{BD})}}$$  \hspace{1cm} (S2)$$

where $pK_a(\text{His})$ and $pK_a(\text{BD})$ are the $pK_a$ of the acidic form of the His side-chain and of the conjugate acid BD of the base that accepts the deuteron from His, that is $D_3O^+$, $D_2O$, or $BufD$, respectively. For the following estimates, we ignore the H/D isotope effect, which largely cancels out in the $pK_a$ difference in Eq. (S2).

Taking $k_D = 10^{10} \text{ M}^{-1} \text{ s}^{-1}$ (probably an overestimate), $pK_a(\text{His}) = 6.38$ (the average of the values in the second $pK^*_a$ column in Table S2), $pK_a(H_3O^+) = -1.74$, and $[D_2O] = 55$ M, we obtain $k_w = 2.4 \times 10^3 \text{ s}^{-1} \approx (240 \mu\text{s})^{-1}$. This estimate is close to the value, $k'_w = 4.2 \times 10^3 \text{ s}^{-1} \approx (240 \mu\text{s})^{-1}$, measured by NMR for imidazole in $\text{H}_2\text{O}$ at 25 °C. For the hydroxide-catalyzed process, with $pK_a(H_2O) = 15.74$, we obtain the estimate $k_b = k_D = 10^{10} \text{ M}^{-1} \text{ s}^{-1}$. With $pK_a(D_2O) = 14.95$ at 25 °C, we then obtain, at pH 7.0, $k_b[OD^-] = 10^{10} \times 10^{7.0-14.95} \text{ s}^{-1} \approx 1.1 \times 10^2 \text{ s}^{-1} = (9 \text{ ms})^{-1}$.

To make a significant contribution to the dominant component of the $^2\text{H}$ MRD profile (Fig. 2a), with a correlation time of $\sim 5 \mu\text{s}$, the mean survival time $\tau_{LD}$ of the labile His deuterons must also be $\sim 5 \mu\text{s}$. Our rough but conservative estimates show that the water and hydroxide catalyzed processes are too slow to contribute significantly. The buffer catalyzed
process can also be ruled out, since a tenfold increase of the phosphate buffer concentration (from 5 to 50 mM) has no significant effect on \( R_1(0) \) (Fig. 2b). Furthermore, at 50 mM buffer, no variation in \( R_1(0) \) was observed between the phosphate (\( pK_a = 7.20 \)), PIPES (\( pK_a = 6.76 \)), and MES (\( pK_a = 6.15 \)) buffers.

A remaining possibility is an internal catalysis such as \( \geq ND^+ \cdots O_w D \cdots OOC \), where a water molecule connects the acidic His side-chain with a nearby proton acceptor, such as a carboxylate group or a basic His side-chain. The crystal structure of equine MbCO suggests several such possibilities (Fig. S1). For example, His-36 has an upshifted \( pK_a \) (Table S2), presumably due to the proximity of Glu-38, the carboxylate group of which is bridged to His-36 via a H-bonding water molecule (Fig. S1a).

![Figure S1](image)

**Figure S1.** Possible internal catalysis of labile-deuteron exchange for (a) His-36, (b) His-97, and (c) His-24/His-119 and His-113/His-116. A red sphere represents a crystallographically identified water molecule.
S2. pD-Dependent Effective Correlation Time

The overall correlation time, $\tau_C$, deduced from one-component fits to solution $^2$H MRD profiles (Fig. 3), decreases with pD even though $\tau_C^{\text{eff}}$ for the LDs increases with pD according to Eq. (3). This happens because LDs make a larger relative contribution to the MRD profile at higher pD. To understand this qualitatively, consider a single class of LDs with pD-dependent mean survival time $\tau_S(pD)$. In view of Eq. (3), we then have approximately

$$\frac{\tau_C}{\tau_R} = \frac{N_W + N_{LD}/A}{N_W + N_{LD}/\sqrt{A}} ,$$

(S3)

with

$$A = 1 + \omega^2 Q^2 S_{iso}^2 \tau_R \tau_S(pD) .$$

(S4)

This heuristic expression predicts that $\tau_C = \tau_R$ at low pD, where $\tau_S$ is so long that the LD contribution is negligible compared to the internal-water contribution. With increasing pD, $\tau_S$ is shortened by base-catalyzed LD exchange. As a result, $\tau_C$ becomes progressively shorter than $\tau_R$, as predicted by Eq. (S3). At still higher pD, $\tau_C$ exhibits a minimum and finally, when $\tau_S$ is so short that $A = 1$, $\tau_C$ again approaches $\tau_R$. In practice, the minimum is not observed (at least not in our pD range) because new classes of LDs with smaller exchange rate constants gradually come into play as pD is increased.
**Figure S2.** Reduced $\chi^2$ and $P(\chi^2)$ for constrained fits to $^2$H MRD profile from immobilized MbCO at pD 7.0 with $N_1$ for component 1 fixed in the fit.

**Figure S3.** Amplitude parameter $NS_{iso}^2$ from single-component fit to the solution $^2$H MRD profile at pD 7.0 (blue line) and computed from the parameters of components 1 and 2 in constrained fits (fixed $N_1$) to the gel $^2$H MRD profile at pD 7.0 (red circles).
S3. Mutual Consistency of $^2$H and $^{17}$O MRD Results

Here, we show that the parameters of the single component in the solution $^{17}$O MRD profile is consistent with the results deduced from the gel $^2$H and $^{17}$O MRD profiles. To a good approximation, the product of the amplitude parameter and correlation time for the single $^{17}$O solution MRD component can be expressed in terms of the parameters of the two components (identified in the gel MRD profiles) that it comprises:

$$NS^2_{iso} \tau_C = \frac{N^{W}_1 S^2_{iso,1} \tau_R}{1 + \omega_Q^2 S^2_{iso,1} \tau_R \tau_{S,1}} + N^W_2 S^2_{iso,2} \left[ \frac{1}{\tau_R} + \frac{1}{\tau_{S,2}} \right]^{-1}. \quad (S5)$$

From the fit results in Table 1, we know that $NS^2_{iso} \tau_C = 16.8 \pm 0.8$ ns and that the second term on the right-hand side of Eq. (S5) equals $8.3 \pm 0.8$ ns. The two components thus make comparable contributions to the solution $^{17}$O MRD profile. In the first term on the right-hand side of Eq. (S5), we know that $\omega_Q = 7.61 \times 10^6 \text{ rad s}^{-1}$, $\tau_R = 11.1$ ns, and $\tau_{S,1} = 5.6$ µs (Table 1). In Eq. (S5), $S_{iso,1}$ refers to the $^{17}$O order parameter, which may differ somewhat from the $^2$H order parameter, $S_{iso,1} = S_1 (1 + \eta_1^2/3)^{1/2} = 0.80 \pm 0.02$ (Table 1). The $^2$H order parameter pertains to internal water molecules as well as to rapidly exchanging LDs in a few His residues (Sec. 3.2).

From our analysis of the pD dependence of the gel $^2$H MRD profiles, we estimated that component 1 comprises $N^W_1 = 5.2 \pm 0.6$ internal water molecules (Sec. 3.2). This result might be affected by modest systematic errors due to the strong covariance of $N_1$ and $\tau_{S,1}$ in the gel $^2$H MRD fit and to inaccuracies in our analysis of the His LD contribution (Sec. 3.2). If our analysis of the gel $^2$H and $^{17}$O MRD profiles is quantitatively consistent, Eq. (S5) should be satisfied with $N^W_1 = 5.2$ and a reasonable $^{17}$O order parameter $S_{iso,1}$. Figure S4 shows that Eq. (S5) is satisfied for $^{17}$O $S_{iso,1}$ values from below 0.5 up to 0.83 when the propagated measurement errors are taken into account. Nonetheless, over most of this $S_{iso,1}$ range, Eq. (S5) predicts a smaller $N^W_1$ value than the one deduced from the pD dependence of the gel $^2$H MRD profiles. The $^{17}$O order parameter is not likely to be substantially smaller than the $^2$H order parameter. Assuming that $S_{iso,1} = 0.80$ also for $^{17}$O, we obtain $N^W_1 = 3.9 \pm 0.6$ from Eq. (S5) (Fig. S4). Taking all available MRD data into account by averaging these two $N^W_1$ values, we arrive at the more conservative estimate $N^W_1 = 4.5 \pm 1.0$. 

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Figure S4. The number $N_{1W}$ of internal water molecules with MST 5.6 µs, deduced with the aid of Eq. (S5) from the solution and gel $^{17}$O MRD profiles, as a function of the $^{17}$O order parameter $S_{\text{iso,1}}$ (blue curve). Also shown is the $N_{1W}$ value obtained from the pD-dependent gel $^2$H MRD profile (red line). The dotted curves or lines indicate the propagated measurement error.
S4. Determination of Xenon Occupancies

The Xe binding constants for equine Mb in the ferrous state at pH 7.0 and 25 °C have been reported as \( K_1 = 94 \text{ M}^{-1} \) for the Xe1 site and \( K_2 = 2.6 \text{ M}^{-1} \) for the weaker sites Xe2 – Xe4 (treated as one site). We compute the Xe occupancy as

\[
\theta_n = \frac{K_n[Xe]}{1 + K_n[Xe]},
\]  

(S6)

where \( n = 1 \) or 2 and [Xe] is the free Xe concentration. We used \(^{129}\text{Xe}\) NMR to determine the total Xe concentration \( C_{\text{Xe}} = [\text{Xe}] + \theta C_{\text{Mb}} \), where \( \theta = \theta_1 + \theta_2 \) and \( C_{\text{Mb}} = 1.62 \text{ mM} \) is the total MbCO concentration in the gel sample.

To determine \( C_{\text{Xe}} \) in the MbCO gel sample, we recorded \(^{129}\text{Xe}\) NMR spectra (Fig. S5) from the gel equilibrated with 8 bar Xe and, for calibration purposes, from two reference samples (50 mM PIPES buffer in D\(_2\)O at pD 7.4 and cyclohexane) equilibrated with 1 atm Xe. The integrated intensity \( I_{\text{Xe}} \) of the Xe peak is proportional to the total Xe concentration \( C_{\text{Xe}} \) in the sample, but it also depends on the sample volume \( V \) (in the active region of the RF coil), the number \( N_S \) of accumulated scans (transients), the \(^{129}\text{Xe}\) longitudinal relaxation rate \( R_{1\text{Xe}} \), and the recycle delay \( \tau_{\text{RD}} \) according to

\[
I_{\text{Xe}} \propto C_{\text{Xe}} V N_S [1 - \exp(-R_{1\text{Xe}} \tau_{\text{RD}})].
\]  

(S7)

The values of these parameters, along with the reported Xe concentration in the reference solvents (at 25 °C and 1 atm Xe) are collected in Table S3. The resulting total Xe concentrations \( C_{\text{Xe}} \) are given in Table S4 with errors propagated from the quoted intensity errors and an estimated 50 % uncertainty in \( R_{1\text{Xe}} \) for the MbCO gel sample. The Xe occupancies \( \theta_1 \) and \( \theta_2 \) were then computed iteratively with the aid of Eq. (S6). In the main text, we use occupancies that are the averages of the values obtained with the two reference samples.
Figure S5. Natural abundance $^{129}$Xe spectra recorded at 14.4 T and 25.0 °C from MbCO gel (8 bar Xe) and from the two reference samples, PIPES buffer and cyclohexane (1 atm Xe). The spectra are scaled to the same $N_S = 256$ and, in addition, the spectrum from cyclohexane was multiplied by 0.1. The $^{129}$Xe chemical shift scale is referenced to the PIPES buffer sample.

Table S3. Parameters Used for Determining Xe Concentrations.

| sample          | $I$ (a.u.) | $C_{\text{Xe}}$ (mM) | $V$ (µl) | $N_S$ | $\tau_{\text{RD}}$ (s) | $R_1^{\text{Xe}}$ (s$^{-1}$) |
|----------------|------------|----------------------|----------|-------|------------------------|-------------------------------|
| MbCO gel       | 105.5 ± 1.1 | –                    | 530      | 2560  | 20.0264                | 0.033$^a$                     |
| 50 mM PIPES    | 1.678 ± 0.185 | 4.5$^b$             | 720      | 256   | 300.0264               | 1.98 × 10$^{-3}$ $^c$          |
| cyclohexane    | 33.77 ± 0.083 | 192$^d$             | 710      | 128   | 60.0264                | 0.017$^e$                     |

$^a$ Estimated from $^{129}$Xe spectra with different $\tau_{\text{RD}}$.  
$^b$ Ref. 9  
$^c$ Ref. 10  
$^d$ Ref. 11  
$^e$ Ref. 12
Table S4. Xenon Concentration and Site Occupancies in MbCO Gel Sample.

| reference     | $C_{\text{Xe}}$ (mM) | occupancy, $\theta_n$ |
|---------------|------------------------|-----------------------|
|               |                        | Xe1       | Xe2 – Xe4  |
| 50 mM PIPES   | 34.2 ± 13.2            | 0.76 ± 0.07 | 0.08 ± 0.03 |
| cyclohexane   | 51.6 ± 18.8            | 0.83 ± 0.05 | 0.12 ± 0.04 |
| average       |                        | 0.80 ± 0.09 | 0.10 ± 0.05 |

Table S5. Results of Fits to $^2$H MRD Profiles from Immobilized MbCO at pD 7.2 and 25 °C with and without 8 bar Xe.$^a$

| parameter (unit) | $-\text{Xe}$ | $+\text{Xe}$ |
|------------------|---------------|---------------|
| $\tau_{C,1}$ (µs) | 5.6 ± 0.8     | [5.6]         |
| $N_1$            | [6.3]         | 6.32 ± 0.03   |
| $S_1$            | 0.78 ± 0.02   | [0.78]        |
| $\eta_1$        | 0.4 ± 0.2     | [0.4]         |
| $\tau_{C,2}$ (ns) | 127 ± 17      | [127]        |
| $N_2 S_{iso,2}^2$ | 0.69 ± 0.05   | 0.71 ± 0.2    |
| $\tau_{C,3}$ (ns) | 6.5 ± 1.3     | [6.5]        |
| $N_3 S_{iso,3}^2$ | 3.8 ± 0.8     | 3.6 ± 0.3    |
| $\xi_H$        | 8.1 ± 0.8     | 8.3 ± 0.6    |
| $\chi^2_{\text{red}}$ | 3.15          | 2.38         |

$^a$ Due to slightly larger data scatter, a constrained fit was performed to the MRD profile in the absence of Xe, with $N_1 = 6.3$ fixed at the value expected from the pD 7.0 fit (Fig. 2a) and His pK$_a$ values (Table S2). For the MRD profile in the presence of Xe, the unconstrained parameter values do not differ significantly from those obtained in the absence of Xe, demonstrating that the two data sets are indistinguishable within experimental error.
Figure S6. Internal water molecules (red spheres) in crystal structures of (a) equine MbCO (PDB: 1DWR) and (b) sperm whale MbCO (PDB: 1A6G) at cryogenic temperature.
**Table S6.** Internal Water Molecules in Crystal Structures of Horse Heart Mb.

| PDB   | form       | res. (Å) | T (K) | pH | internal water characteristics                                      |
|-------|------------|----------|-------|----|---------------------------------------------------------------------|
|       |            |          |       |    | site (water no.) | occup. | B factor | H-bond acceptor/donor (length in Å) |
| 1HRM² | H93Y, met? | 1.70     | n/a   | n/a| Xe3a (160)         | 1.0    | 18.25    | I75 O (2.9), G80 N (2.8), H82 Nδ¹ (2.9), Xe3b (3.4) |
|       |            |          |       |    | Xe3b (159)         | 1.0    | 34.00    | A134 O (2.8), Xe3a (3.4)                |
| 1WLA³ | met        | 1.70     | n/a   | n/a| DP (156)           | 1.0    | 8.26     | Heme Fe, H64 Nε²                           |
|       |            |          |       |    | Xe3a (180)         | 1.0    | 10.89    | I75 O (2.9), G80 N (2.7), H82 Nδ¹ (3.0), Xe3b (3.0) |
|       |            |          |       |    | Xe3b (216)         | 1.0    | 38.98    | A134 O (3.1), Xe3a (3.0)                |
|       |            |          |       |    | apical (217)       | 1.0    | 36.46    | Q26 Nε² (2.6), M55 O (2.7), S58 O (3.0) |
| 1DWR⁴ | CO         | 1.45     | 100   | 7.5| Xe3a (2072)        | 1.0    | 10.01    | I75 O (2.9), G80 N (2.8), H82 Nδ¹ (2.8), Xe3b (3.0) |
|       |            |          |       |    | Xe3b (2106)        | 1.0    | 18.53    | A134 O (3.0), Xe3a (3.0)                |
|       |            |          |       |    | apical (2059)      | 1.0    | 13.91    | Q26 Nε² (2.7), M55 O (2.8), S58 O (2.6) |
|       |            |          |       |    | bottom (2078)      | 1.0    | 13.00    | Q91 Nε² (3.2), K145 O (3.0), E148 Oε¹ (2.9) |
| 2V1R⁵ | deoxy      | 1.25     | 110   | 6.8| DP (2186)          | 1.0    | 32.80    | Heme Fe (3.7), H64 Nε² (3.6)           |
|       |            |          |       |    | Xe3a (2100)        | 1.0    | 14.13    | I75 O (2.8), G80 N (2.9), H82 Nδ¹ (2.8), Xe3b (3.0) |
|       |            |          |       |    | Xe3b (2155)        | 1.0    | 20.92    | A134 O (3.0), Xe3a (3.0)                |
|       |            |          |       |    | apical (2038)      | 1.0    | 20.87    | Q26 Nε² (2.6), M55 O (2.8), S58 O (2.7) |
|       |            |          |       |    | bottom (2172)      | 1.0    | 16.89    | Q91 Nε² (2.9), K145 O (3.0), E148 Oε¹ (2.6) |
### Table S7. Internal Water Molecules in Crystal Structures of Sperm Whale Mb.

| PDB   | form | res. (Å) | T (K) | pH | site (water no.) | occup. | B factor | H-bond acceptor/donor (length in Å)        |
|-------|------|----------|-------|----|-----------------|--------|----------|------------------------------------------|
| 1BZR  | CO   | 1.15     | 287   | 5.9| Xe3a (340)      | 1.0    | 18.25    | I75 O (2.8), G80 N (2.9), H82 N\textsuperscript{81} (2.8), Xe3b (3.1) |
|       |      |          |       |    | Xe3b (403)      | 1.0    | 31.34    | A134 O (3.1), Xe3a (3.1)                 |
|       |      |          |       |    | apical (304)    | 0.65   | 18.07    | Q26 N\textsuperscript{c2} (2.9), M55 O (2.7), S58 O (2.7) |
|       |      |          |       |    | W1 (382)        | 1.0    | 26.32    | A22 O (2.7), K62 O (2.6)                 |
| 1A6G  | CO   | 1.15     | 100   | 6.0| Xe3a (1006)     | 0.86   | 11.34    | I75 O (2.8), G80 N (2.9), H82 N\textsuperscript{81} (2.8), Xe3b (3.0) |
|       |      |          |       |    | Xe3b (1056)     | 0.88   | 17.29    | A134 O (2.9), Xe3a (3.0)                 |
|       |      |          |       |    | apical (1053)   | 1.0    | 14.96    | Q26 N\textsuperscript{c2} (2.6–2.9), M55 O (2.9), S58 O (2.8) |
|       |      |          |       |    | W1 (1011)       | 0.86   | 16.32    | A22 O (2.6), K62 O (2.7)                 |
|       |      |          |       |    | W2 (1154)       | 0.71   | 30.44    | A127 O (2.7)                             |
| 1BZ6  | met  | 1.20     | 287   | 6.0| DP (389)        | 1.0    | 8.86     | Heme Fe (2.2), H64 N\textsuperscript{c2} (2.7) |
|       |      |          |       |    | Xe3a (352)      | 1.0    | 12.75    | I75 O (2.8), G80 N (2.9), H82 N\textsuperscript{81} (2.8), Xe3b (3.1) |
|       |      |          |       |    | Xe3b (417)      | 1.0    | 34.98    | A134 O (3.1), Xe3a (3.1)                 |
|       |      |          |       |    | apical (509)    | 0.30   | 11.87    | Q26 O\textsuperscript{c1} (2.9), M55 O (2.8), S58 O (2.8) |
|       |      |          |       |    | W1 (393)        | 1.0    | 19.83    | A22 O (2.7), K62 O (2.7)                 |
|       |      |          |       |    | W2 (500)        | 0.50   | 24.49    | A127 O (3.0)                             |
| 1A6K  | met  | 1.10     | 90    | 7.0| DP (1001)       | 1.0    | 9.70     | Heme Fe (2.1), H64 N\textsuperscript{c2} (2.7) |
|       |      |          |       |    | Xe3a (1006)     | 0.93   | 10.64    | I75 O (2.8), G80 N (2.8), H82 N\textsuperscript{81} (2.7), Xe3b (3.0) |
|       |      |          |       |    | Xe3b (1056)     | 0.83   | 14.77    | A134 O (2.9), Xe3a (3.0)                 |
|       |      |          |       |    | apical (1053)   | 1.0    | 11.55    | Q26 N\textsuperscript{c2} (2.6–3.0), M55 O (2.9), S58 O (2.8) |
|       |      |          |       |    | W1 (1011)       | 0.93   | 13.02    | A22 O (2.7), K62 O (2.7)                 |
|       |      |          |       |    | W2 (1154)       | 0.70   | 23.42    | A127 O (2.9)                             |
Figure S7. Arrhenius plot of the MST $\tau_{S,1}$ for component 1 in the $^2$H MRD profile from immobilized MbCO at the indicated pD values. The slope yields $E_A = 17.4 \pm 0.4$ kJ mol$^{-1}$ at pD 7.0 and $17.0 \pm 0.3$ kJ mol$^{-1}$ at pD 6.6.
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