Optical trapping by petal-like circular Airy beam

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Abstract. Superposition of two circular Airy vortex beams (CAVB), with opposite sign topological charges (ℓ), produces a new type of petal beams called petal-like circular Airy beam (PCAB) with a transverse field distribution in the form of azimuthally modulated concentric rings that follow Airy function over the radial distance on a transverse plane. In this paper, tight focusing of truncated PCAB and its application in optical trapping is numerically investigated. It is shown that by adjusting the beam parameters four different trapping configurations can be achieved: a single transverse trap at a single axial position, a multi-trap geometry at a single axial position, two single transverse traps at two positions along the axial direction, and two multi-trap geometries at two different axial positions. It is also shown that the number of trapped particles in the multi-trap configurations is 2ℓ per focal plane, while the number of axial trap positions is determined by the truncation aperture size. Finally, trap stiffnesses and corresponding potential energies for the trapping configurations are presented and discussed.
1. Introduction

Due to their peculiar propagation characteristics such as diffraction-free propagation, self-acceleration [1], and self-healing [2], optical Airy beams have attracted extensive attention, and rapidly drawn research interests in various applications such as filamentation [3, 4], particle clearing [5], optical micro- and nano-manipulation [6, 7], and light-sheet fluorescence microscopy [8, 9]. Several other optical beams have been designed in a way that they exhibit features of Airy beam in specific manners. Especially, beams with abrupt autofocusing property, inherited from the self-acceleration property of Airy beam, are of particular importance in several applications; circular Airy beam (CAB) [10], orbital angular momentum (OAM)-carrying circular Airy vortex beam (CAVB) [11], vector circular Airy beam (VCAB) with a cylindrically symmetric polarization distribution [12], radially polarized symmetric Airy beam [13], circular Airy beam with a Gaussian envelope [14], elliptical Airy beam [15], and Tornado waves [16] are examples of such beams. Zhu et al. have shown that the number of axial focal positions of a tight focusing CAB can be tuned by adjusting the beam parameters and the radius of a hard aperture that determines the beam extension [17]. Zhuang et al. have shown that a tightly focused CAVB has a ring-shaped transverse focal spot whose radius is determined by the topological charge (TC) of the beam [18]. Owing to their abrupt autofocusing feature, these beams have found applications in optical manipulation. There are several reports on the use of these beams in optical trapping of various particles, such as optical manipulation of Mie particles [19], optical trapping of two types of particles with lower and higher refraction indices with respect to a surrounding medium [20], trapping of Rayleigh particles [21], the formation of two axial traps by tightly focused circularly polarized CAB [22], and optical trapping and rotation of micro-particles by CAVB [23]. In 2017, Porfirov and Khonina demonstrated an azimuthally modulated circular superlinear Airy beam, as a general form of petal-like CAB [24]. The electric field envelope of the beam was considered as circular Airy function with a certain power order carrying a vortex of a certain TC, and modulated by a “circ” function. They studied the abrupt autofocusing and self-healing properties of the beam for different values of the power order and TC.

Petal-like circular Airy beams (PCABs) are a linear superposition of two CAVBs with opposite sign TCs. The transverse intensity profile of this beam is composed of azimuthally modulated petal-shaped concentric rings whose radial profile follows Airy function, while the number of petals is determined by TC. These beams also exhibit self-healing and abrupt autofocusing properties that make them a good candidate for optical micro- and nano-manipulation applications. Moreover, by adjusting the truncation aperture of the beam at an initial plane and choosing a proper TC, the geometry of three-dimensional traps formed by tightly-focused PCAB can be adjusted. In this paper, tight focusing of PCAB with different values of TC is investigated, and it is shown that by adjusting the radius of truncation aperture (aperture of the focusing lens) and other beam parameters, the focal intensity distribution can be tuned, and hence several configurations for the generated optical traps can be achieved, including a single or dual axial trap geometry with single or multiple transverse trapping sites. Generalized Lorenz-Mie theory (GLMT) is used for investigating the optical trap formation by tightly focused PCAB for sub-micron particles, and eventually, the traps are characterized in terms of their stiffness and potential energy. These findings may be found useful in the design and optimization of optical tweezers and micro-, nano-manipulation applications.

2. Theoretical approach

In this section, the formation and tight focusing of PCAB is briefly discussed, and GLMT formalism for the calculation of optical forces by using Maxwell’s stress tensor is presented.

2.1. Petal-like circular Airy beam (PCAB)

Circular Airy vortex beam (CAVB) is a solution of the vector Helmholtz equation in the paraxial regime [11, 18, 23]. The electric field envelope of CAVB is given as

\[ \mathbf{E}^{(l)}_{\text{CAVB}}(\rho, \varphi) = E_0 \text{Ai} \left( \frac{\rho_0 - \rho}{w} \right) \exp \left( a \frac{\rho_0 - \rho}{w} \right) \times \exp(i l \varphi) \mathbf{\hat{e}}, \]

(1)

where \( E_0 \) is an initial amplitude, \( \text{Ai}(\cdot) \) denotes Airy function, \( \rho \) and \( \varphi \) are radial and azimuthal coordinates in a transverse plane, respectively; and \( \rho_0, w, a, l, \) and \( \mathbf{\hat{e}} \) represent the radius of the first ring of the beam, a scaling factor (that determines the width of the rings), an exponential decay factor, topological charge, and polarization state, respectively.

Petal-like circular Airy beams (PCAB) are a coherent superposition of two CAVBs with identical beam parameters but opposite sign TCs. As a result, the beam will possess 2l main petals, and its electric field at an initial distance (\( z = 0 \)) can be written as [24]:

\[ \mathbf{E}^{(2l)}_{\text{PCAB}} = \mathbf{E}^{(l)}_{\text{CAVB}} + \mathbf{E}^{(-l)}_{\text{CAVB}}. \]

(2)

Transverse intensity profiles of two PCABS with \( l = 0 \) and \( l = 3 \) are illustrated in figures 1(a) and...
transformation. For a given set of other beam parameters. Throughout this work, we investigate four combinations of the choices of \( l \) and \( R \), while other parameters are selected as \( \lambda = 1064 \text{ nm}, \rho_0 = 1 \text{ mm}, w = 0.095 \text{ mm} \) and \( a = 0.01 \). Moreover, the beam power is set to a constant value of 100 mW in all cases.

Figures 1(b) and 1(c) show the transverse intensity profiles of a truncated PCAB with \( l = 0 \), for \( R = 1.23 \text{ mm} \) and \( R = 1.4 \text{ mm} \), respectively. The transverse intensity profiles of PCAB with \( l = 3 \) and the same truncation apertures are demonstrated in figures 1(e) and 1(f), respectively. Clearly, for \( R = 1.23 \text{ mm} \), only the first (main) ring of the PCABs is permitted to be focused by the lens while for \( R = 1.4 \text{ mm} \) both the main ring and a secondary ring reach the focusing lens.

2.2. Beam focusing

In the optical trapping process, the incident light beam is strongly focused to a diffraction-limited spot. According to Debye vectorial diffraction theory [25], the electric field distribution of a focused beam can be expressed as

\[
E_f(r) = A_0 \int_0^\alpha \sin \theta \int_0^{2\pi} E_{\text{t},t}(\theta, \varphi) e^{i(k_f \tau d\varphi - x \cos \theta)} d\theta,
\]

where \( k = n k_0 \) is the wavenumber in the propagation medium, \( n \) is the refractive index of the medium, \( k_0 \) is the wavenumber in vacuum, \( f \) is the focal length of the lens, \( \alpha \) is the maximum convergence angle in the medium, and \( (\theta, \varphi) \) are the polar and azimuthal coordinates in a spherical coordinate system centered at the focus. Additionally, \( E_{\text{t},t}(\theta, \varphi) \) is the transmitted far-field distribution of the electric field of the beam, given as [26]

\[
E_{\text{t},t}(\theta, \varphi) = \left( t_s(\theta) \left[ E_{\text{PCAB}}^{(2)}(\rho, \varphi) \cdot \hat{\theta} \right] \hat{\varphi} + t_p(\theta) \left[ E_{\text{PCAB}}^{(2)}(\rho, \varphi) \cdot \hat{\rho} \right] \hat{\theta} \right) \sqrt{\cos \theta},
\]

where \( t_s(\theta) \) and \( t_p(\theta) \) are the Fresnel transmission coefficients of the lens for perpendicular and parallel polarization states, respectively. Here, \( \hat{\rho} \) and \( \hat{\varphi} \) are the radial and azimuthal unit vectors of a cylindrical coordinate system whose \( z \)-axis is along the propagation direction of the beam before the lens, while \( \hat{\theta} \) and \( \hat{\varphi} \) are the polar and azimuthal unit vectors of the spherical coordinate system after the lens, respectively. The calculated axial (\( x-z \)) and lateral (\( x-y \)) focal intensity distributions of the focused PCABs with several \( l \) values \( l = 0, 1, 2, 3, 4 \), and two truncation apertures of \( R = 1.23 \text{ mm} \) and \( R = 1.4 \text{ mm} \), with \( n = 1.33 \) and \( \alpha = 60^\circ \) (i.e. \( \text{NA} = 1.3 \), for both truncation aperture sizes), are depicted in figure 2. We have assumed spherical aberration to be negligible here. As it can be seen, for \( R = 1.23 \text{ mm} \), and all TCS, the beam is focused in a single axial point (i.e. on a single transverse \( x-y \) plane), while for \( R = 1.4 \text{ mm} \), the beam forms two axial focus positions (i.e. on two \( x-y \) focal planes with a longitudinal distance determined by \( w \) and \( f \)). Moreover, for \( l = 0 \) and both truncation apertures, the beam forms a single round focal spot in the transverse focal plane(s), while for \( l \neq 0 \) multiple discrete petal-shaped structures are formed in the focal plane(s), with \( 2l \) petals located on a circle around the optical axis (clearly noticeable for higher values of \( l \)). The diameter of the circle also depends on \( l \) and increases by increasing \( l \). Quantitively, for \( R = 1.23 \text{ mm} \), the diameter of the petal-shaped structure, increases from 0.55 \( \mu \text{m} \) for \( l = 1 \) to 1.6 \( \mu \text{m} \) for \( l = 4 \). It is emphasized here that for \( R = 1.4 \text{ mm} \), the transverse intensity distribution is almost identical on both focal planes, which are separated by an axial distance of \( \sim 2.5 \mu \text{m} \). Also, in a similar manner to the previous case, the diameter of the petal-shaped
figure 2. Longitudinal (x − z) and transverse (x − y) focal intensity distribution for R = 1.23, and 1.4 mm and different values of l. Depicted intensity profiles are individually normalized to their corresponding peak value for a better visual comparison of the focused beam structures. For quantitative comparison of the peak intensity for each case, the peak intensity corresponding to the case of l = 0 and R = 1.23 mm, is considered as a reference intensity scale, and the peak intensity of the depicted profiles with respect to the reference intensity scale is indicated by the intensity scale (IS) values.

Moreover, for a better visual comparison of the focused beam structures, all intensity profiles in figure 2 are individually normalized to their corresponding peak intensity. However, for a quantitative comparison of the maximum intensity for different configurations, we considered the peak intensity achieved for R = 1.23 mm, and l = 0 as a reference intensity scale (IS). The peak intensities of the other cases, with respect to the reference intensity scale, are indicated on their focal intensity profiles. Understandably, the peak intensity is considerably reduced for the larger R and higher values of l, since the beam power is divided among multiple axial/lateral focal spots.

It should also be added that a bigger truncation aperture size, would lead to the formation of additional axial focal positions, as expected for a regular CAB [10]. However, even for a very small exponential decay factor, a, (such as the selected value of 0.01), as the radius of the peripheral rings increases, the peak intensity is reduced and the intensity contrast between the extra axial focal points, formed by those additional rings is diminished, and they eventually form a focal line. Therefore, allowing only a few first rings to form the focus would suffice for the formation of stable three-dimensional traps. Also, the effect of higher values for the exponential decay factor would be similar to the effect of a smaller truncation aperture size, with some minor differences. On the other hand, the radius of the main ring $p_0$, and its width, which is determined by the scaling factor $w$, determine the longitudinal, and lateral extensions of the focal region under the action of autofocusing in free space.

2.3. Optical force

Calculation of the net optical force exerted on spherical particles by a focused optical beam can be rigorously performed by using the generalized Lorenz-Mie theory (GLMT) and Maxwell’s stress tensor. The first step in this procedure is the calculation of the scattered field from the particle(s) based on the GLMT. For this purpose, both the incoming and scattered electric fields are expanded in terms of electric and magnetic multipole fields [27]

$$E_i = \sum_{pn'm'} A^{(p)}_{n'm'} J^{(p)}_{n'm'};$$

$$E_s = \sum_{pn'm'} A^{(p)}_{n'm'} H^{(p)}_{n'm'},$$

where $J^{(p)}_{n'm'}$, and $H^{(p)}_{n'm'}$ are the multipole fields of the incoming, and scattered electric fields, respectively, (expressed in terms of the vector spherical harmonics), $p = 1$ and $p = 2$ denote the magnetic and electric multipoles, respectively, $n'$ determines the order of multipoles in the expansion and changes in the range of 0 to $n'_{max}$ (that is determined by Wiscombe criterion [26]), and $m' = -n', \ldots, n'$. Finally, $\mathcal{W}^{(p)}_{n'm'}$ and $\mathcal{A}^{(p)}_{n'm'}$ are the expansion coefficients of the incoming and scattered fields, respectively. It is worth noticing that, for a spherical particle, once the expansion coefficients of the incident focused beam are found through the multipole expansion of plane waves in relation (3), the expansion coefficients of the scattered field can be obtained by using the transfer matrix of a spherical particle, as [27]

$$\mathcal{A}^{(1)}_{n'm'} = b_n \mathcal{W}^{(1)}_{n'm'},$$

$$\mathcal{A}^{(2)}_{n'm'} = a_n \mathcal{W}^{(2)}_{n'm'},$$

where $b_n$ and $a_n$ are the main diagonal elements of the transfer matrix (or the Mie coefficients) of the spherical particle and depend on the diameter, $D_p$, and the refractive index, $n_p$, of the particle.

In order to calculate the net optical force exerted on a particle, numerical integration of the time-averaged Maxwell stress tensor, $\langle\mathcal{T}_M\rangle$, should be performed over a spherical surface ($A$) encircling the particle [26, 27]

$$F = \int_A \langle\mathcal{T}_M\rangle \cdot \hat{n} \, ds,$$
where
\[
\langle T_M \rangle = \frac{1}{8\pi} \text{Re} \left\{ n^2 E E^* + B B^* - \frac{1}{2} (n^2 |E|^2 + |B|^2) \right\}.
\]
Here \( \hat{n} \) is a unit vector perpendicular to surface \( A \); \( n \) is the refractive index of the surrounding medium, \( I \) is the unit dyadic, and the symbol * denotes the complex conjugation. \( B = B_i + B_s \) and \( E = E_i + E_s \) are the total magnetic and electric fields, respectively, which are interrelated through \( B = -(i/k) \nabla \times E \). Thus, the magnetic fields can be calculated when the corresponding electric fields are found using relation (4).

It is convenient to consider the optical force exerted on a trapped particle as a restoring spring force around an equilibrium position as [28]
\[
F_i = -k_i \Delta i \quad i = r, z,
\]
where \( r, z \) represent the lateral and axial distances from an equilibrium position, respectively, and \( k_i \) denotes the trap stiffness along each direction. Therefore, a stronger trap is expected to have greater stiffness. Additionally, following the same analogy, a potential well can be attributed to an optical trap with energy given by [29]
\[
U_i = -\int_{-\infty}^{\infty} F_i \, di \quad i = r, z.
\]
A deeper potential well is associated with reduced kinetic fluctuations related to the Brownian motion of a trapped particle. The minimum depth of potential well (DPW) should be at least \( 10 k_B T \) [29], where \( k_B \) is the Boltzmann constant.

3. Results and discussion

According to the mentioned theoretical description, we investigated the optical trapping of sub-micron particles under the irradiation of the focused PCABs. Throughout these investigations, the beam and focusing parameters were maintained as those described in the previous section, and the particles were assumed to be polystyrene (PS) microspheres with a diameter of \( D_p = 500 \) nm, and refractive index of \( n_p = 1.57 \) (at \( \lambda = 1064 \) nm).

Focusing geometry and trapping configurations of PCAB is schematically illustrated in figure 3. Depending on truncation aperture \( R \), one or two rings of the PCAB are allowed to be focused by the lens into the trapping medium. As shown in figure 3(a), for a larger \( R \) and \( l \neq 0 \) (as a general case), two focal planes (p1 and p2) with a separation distance, \( d \), are formed in the focal region. The transverse intensity distribution on each focal plane is composed
of a circular petal-shaped pattern with a diameter of $D$. As schematically depicted, each petal may act as an optical trap, and therefore several particles can be simultaneously trapped in such a multi-trap configuration. By the two choices of $R$ (i.e. $R = 1.23$ mm, and $R = 1.4$ mm), and two category of options for $l$ (i.e. $l = 0$ and $l \neq 0$), four trapping configurations can be achieved, as demonstrated in figure 3(b): a single lateral trap on a single focal plane ($R = 1.23$ mm, and $l = 0$), multiple lateral traps on a single focal plane ($R = 1.23$ mm, and $l \neq 0$), two single lateral traps on two focal planes ($R = 1.4$ mm, and $l = 0$), and finally, multiple lateral traps on two focal planes ($R = 1.4$ mm, and $l \neq 0$).

Figure 4. Diagrams of the axial (a, b), and lateral (c, d), optical forces exerted on a polystyrene microsphere with $D_p = 500$ nm, for two sizes of the truncation aperture $R = 1.23$ mm (a, c), and $R = 1.4$ mm (b, d), and several values of $l$. The yellow filled circles show the trap positions along the axial and lateral directions; for $l = 0$, the lateral trap position is located at $r = 0$.

The calculated axial and lateral optical forces ($F_z$ and $F_r$, respectively) exerted on PS microspheres are shown in figure 4. Clearly, for both truncation apertures, the maximum axial and lateral forces are reduced for higher values of $l$. This is simply due to the fact that by increasing the TC, maximum intensity on each petal of the focused beam is decreased. Moreover, it is seen that maximum lateral forces (among all cases) is higher than the maximum axial force since the beams are sharply localized along with the lateral directions than the axial direction (as it can be seen in figure 2). For instance, the maximum exerted axial force in figures 4(a) and 4(b) is about 8 pN, while in the lateral direction, the maximum exerted force is about 20 pN and 13 pN for $R = 1.23$ and 1.4 mm, respectively, as shown in figures 4(c) and 4(d).

Furthermore, it is seen that for $R = 1.23$ mm, a particle can be trapped at a single focal plane (indicated by the yellow circles in figure 4(a)), while for $R = 1.4$ mm, particle trapping may occur at any of the two focal planes (p1, and p2) as indicated by the yellow circles in figure 4(b). It should also be noted that the maximum axial forces of the single-plane and dual-plane trapping configurations are almost identical, despite the fact that the maximum intensity for $R = 1.23$ mm is higher. This can be understood based on the axial focal intensity distributions shown in figure 2; for $R = 1.23$ mm, the focus is elongated along the propagation direction, while for $R = 1.4$ mm, two discrete and rather localized focal regions are formed. This suggests that the intensity gradient is steeper for the latter case, resulting in a higher axial force.

Additionally, as depicted in figures 4(c) and 4(d), for $l \neq 0$ particle trapping may take place at different lateral positions (indicated by the yellow circles) on the petals of the focused beam whose number and geometry are determined by the value of $l$. It is also seen that the radial distance between the trapping positions for the single plane trapping configuration is slightly smaller than that of the dual-plane configuration. For instance, for $l = 3$ and single-plane trapping configuration, 6 particles can be trapped on a single plane with a circular geometry and a diagonal distance of 1.25 $\mu$m, whereas for $l = 3$ and dual-plane trapping configuration, 12 particles can be trapped on two focal planes (i.e. 6 particles on each plane), with a circular geometry and a diagonal distance of 1.33 $\mu$m.

Figure 5. Calculated trap stiffnesses in (a) axial, and (b) lateral directions as a function of topological charge $l$, for different sizes of truncation aperture.

As stated earlier in Sec. 2, trap stiffness defined through relation (6), can be considered as a quantitative measure of the strength of an optical trap. Calculated stiffnesses for the optical traps indicated in figure 4 in both axial and lateral directions for various trapping configurations are plotted in figure...
5. Obviously, the lateral trap stiffnesses are about an order of magnitude higher than the axial ones. Also, figure 5(a) shows that for \( l = 0 \) dual-plane trapping configuration forms a higher trap stiffness than a single-plane configuration. This is due to smaller and rather localized focal spots along the axial direction in the former case. Additionally, by increasing the value of the TC, trap stiffness is decreased from \( \sim 14 \text{ mN mm}^{-1} \), for \( l = 0 \), to \( \sim 3 \text{ mN mm}^{-1} \), for \( l = 4 \). On the other hand, in the lateral direction, as shown in figure 5(b) the single-plane trapping configuration forms stronger traps for all values of \( l \) due to smaller spot sizes, and higher peak intensities on each petal on the focal plane. Here, the calculated lateral stiffnesses for the dual-plane case are the same on both focal planes, \( p_1 \), and \( p_2 \).

![Figure 6](image_url)  
*Figure 6.* Calculated potential energy of the optical traps and their corresponding depth of potential well (DPW), for different configurations. (a) and (b) show the potential energy diagram for \( R = 1.23 \text{ mm} \), and \( R = 1.4 \text{ mm} \), respectively, in axial direction, while (c) and (d) show the corresponding diagrams in lateral direction.

Moreover, relation (7) was used to calculate the potential energy of the optical traps. The calculated potential energies along axial and lateral directions are shown in figure 6 (\( T = 300 \text{ K} \) is selected in this study). Figures 6(a) and 6(b) show the axial potential energy for the single-, and dual-plane trapping configurations, respectively. It is seen that depth of potential well (DPW), defined as the energy difference between a local minimum and a nearest local maximum, is in general, greater for single-plane configuration than a dual-plane one since in the latter case the beam power is divided into two focal regions (i.e. planes), between at least two focal spots, each on an individual focal plane. For instance, for \( l = 0 \), DPW in the single-plane configuration is about 1500 \( k_B T \), while the corresponding values in the dual-plane configuration are about 600 \( k_B T \), and 1100 \( k_B T \), on \( p_1 \) and \( p_2 \), respectively. The least DPW is achieved for \( l = 4 \) in the first focal plane of the dual-plane configuration, with a value of 125 \( k_B T \); however, this value is still well beyond the minimum DPW required for the formation of a stable trap (10 \( k_B T \)). The lateral potential energies are shown in figures 6(c) and 6(d) for single- and dual-plane trapping configurations, respectively. Obviously, in both cases, single transverse traps (\( l = 0 \)) provide greater DPW than the multiple traps (\( l \neq 0 \)); and higher \( l \) is associated with a further reduced DPW. Also, a comparison of figures 6(c) and 6(d) reveals that the lateral DPW is lower for the dual-plane trapping case. These are attributed to the power division between two focal planes in the case of dual-plane trapping, and further reduction of the peak intensity in each trapping site by increasing the value of \( l \). Furthermore, it is important to note here, when the diagonal distance \( D \) between multiple trapping sites is comparable to the particle diameter \( (D_p) \), multiple transverse potential wells are converted to a single potential well, in a way that the multi-petal beam structure acts equivalently as a single large spot, and hence a single trap is formed with reduced DPW. In our case, \( D_p = 0.5 \mu\text{m} \), while the minimum diagonal distance between trapping sites of \( D = 0.53 \mu\text{m} \) is achieved for \( l = 1 \) with two petals. This indicates that the two particles can almost independently be trapped in each petal with a reduced DPW; however, higher values of \( l \) are associated with larger diagonal distances, and therefore DPW has increased again for \( l > 1 \). On the other hand, a perfect 2\( l \) multiple trap configuration for a petal beam with the topological charge of \( l \) can only be achieved when the particle diameter does not exceed the distance between two adjacent petals, as it is ensured here.

4. Conclusion

In summary, it was shown that a superposition of two circular Airy vortex beams (CAVBs), with opposite sign topological charge, produces a new kind of optical beams called petal-like circular Airy beam (PCAB) that is promising for applications such as optical manipulation. Tight focusing of PCAB for two truncation apertures \( R \) and several values of the topological charge \( l \) is numerically investigated, and it is shown that different combinations of these parameters result in different intensity distributions around the focal region. It is demonstrated that four distinct trapping configurations can be achieved by proper choices of the parameters: (i) A single lateral trap on a single focal plane \( (R = 1.23 \text{ mm} \) and \( l = 0 \);
(ii) A petal-shape lateral multiple-trap geometry on a single focal plane ($R = 1.23$ mm, and $l \neq 0$); (iii) Two single lateral traps on two distinct focal planes ($R = 1.4$ mm, and $l = 0$); and (iv) Two petal-shape lateral multiple-trap geometries on two distinct focal planes ($R = 1.4$ mm, and $l \neq 0$). The trap stiffness ($k$) and the depth of potential well (DPW), for each case, is calculated, and it is discussed that a perfect 2l lateral multiple-trap geometry can be achieved for particle size smaller than the distance between adjacent trap sites. The work may find applications in the implementation of particle trapping, and nano-, micro-manipulation by PCAB and similar azimuthally modulated, abruptly autofocusing beams.

Competing interests

The authors declare no competing interests.

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