Title
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Permalink
https://escholarship.org/uc/item/2dp011w2

Journal
Nano Letters, 21(14)

ISSN
1530-6984

Authors
Berger, Emma
Jamnuch, Sasawat
Uzundal, Can B
et al.

Publication Date
2021-07-28

DOI
10.1021/acs.nanolett.1c01502

Peer reviewed
Extreme Ultraviolet Second Harmonic Generation Spectroscopy in a Polar Metal

Emma Berger,* Sasawat Jamnuch, Can B. Uzundal, Clarisse Woodahl, Hari Padmanabhan, Angelique Amado, Paul Manset, Yasuyuki Hirata, Yuya Kubota, Shigeki Owada, Kensuke Tono, Makina Yabashi, Cuixiang Wang, Youguo Shi, Venkatraman Gopalan, Craig P. Schwartz, Walter S. Drisdell, Iwao Matsuda, John W. Freeland, Tod A. Pascal, and Michael Zuerch*  

ABSTRACT: The coexistence of ferroelectricity and metallicity seems paradoxical, since the itinerant electrons in metals should screen the long-range dipole interactions necessary for dipole ordering. The recent discovery of the polar metal LiOsO₃ was therefore surprising [as discussed earlier in Y. Shi et al., Nat. Mater. 2013, 12, 1024]. It is thought that the coordination preferences of the Li play a key role in stabilizing the LiOsO₃ polar metal phase, but an investigation from the combined viewpoints of core-state specificity and symmetry has yet to be done. Here, we apply the novel technique of extreme ultraviolet second harmonic generation (XUV-SHG) and find a sensitivity to the broken inversion symmetry in the polar metal phase of LiOsO₃ with an enhanced feature above the Li K-edge that reflects the degree of Li atom displacement as corroborated by density functional theory calculations. These results pave the way for time-resolved probing of symmetry-breaking structural phase transitions on femtosecond time scales with element specificity.

KEYWORDS: X-ray nonlinear spectroscopy, polar metal, materials science, second harmonic generation

A central question of condensed matter physics is how the structure of a material gives rise to its function. One approach to this so-called “structure–function problem” is to ask how the elemental composition plays a role in a material’s emergent functionality. A symmetry-based perspective offers yet another valuable viewpoint. Here, we combine the insights of both approaches in a single experiment, namely extreme ultraviolet second harmonic generation (XUV-SHG), to explore the nonintuitive coexistence of polarity and metallicity in lithium osmate (LiOsO₃). Although it was first predicted over 50 years ago that polar metals could form through a second-order phase transition, the first experimentally realized “ferroelectric-like” metal, LiOsO₃, was discovered only recently.² The search for polar metals has since expanded, motivated by prospects of multiferroics, polar superconductors, nonlinear optical media, and thermoelectric devices. Recent works predicting asymmetric hysteresis in LiOsO₃ thin films and revealing ferroelectric switching in a two-dimensional metal¹⁰ have generated significant recent excitement for the practical application of low-dimensional devices. Despite the numerous attempts to explain the coexistence of polarity and metallicity, there are still many unanswered questions as to how polar order can be stabilized in a metal.

Since its discovery, LiOsO₃ has become a prototypical polar metal. In this perovskite-structured material (ABO₃), a continuous order–disorder phase transition occurs at a critical temperature of Tᵰ = 140 K, where it transitions from an R₃c nonpolar metallic to an R₃c polar metallic phase through the loss of inversion symmetry (Figure 1a). Neutron diffraction,¹¹ and optical spectroscopy² have shown that the Aₙₜ soft phonon mode responsible for the transition involves a coordinated 0.5 Å displacement of Li atoms along the polar c-axis.¹¹ To explain these observations, several theories have been developed.¹³−¹⁷ The decoupled electron mechanism hypothesis proposed by Puggioni et al. postulates that the soft phonon responsible for driving the “ferroelectric” transition is energetically decoupled from the electrons at the Fermi level responsible for the metallicity. In this picture, ineffective electron screening of long-range dipolar couplings stabilize the polar phase.⁹,¹²,¹⁸ Benedek et al. proposed a
related mechanism that emphasizes short-range, atomic details. Here, ion-size mismatch effects and the local coordination preferences of the A-site Li atom are thought to drive the phase transition. With short-range interactions at the forefront, the itinerant electrons that are expected to screen the dipole−dipole forces are, thus, of secondary importance. In the high-temperature phase, the Li atom is coordinated to nine nearby O atoms via three short Li−O bonds and six long Li−O bonds. On the other hand, signatures of the polar metal phase include OsO6 octahedral rotations that shorten three of the longer Li−O bonds, and Li atoms displacements that shorten the three short Li−O bonds. On the other hand, signatures of the polar metal phase include OsO6 octahedral rotations that shorten three of the longer Li−O bonds, and Li atoms displacements that shorten the three short Li−O bonds. The overall effect of these structural changes is to octahedrally coordinate the Li atom in the polar metal phase (Figure 1b). With regard to why all the Li atoms are displaced uniformly, their coordinated motion is thought to both minimize the number of faces Li octahedra share with Os octahedra and open up unscreened channels of anisotropic Coulomb interactions by which to minimize the free energy. Hence, the Li-coordination environment plays a determining role in the stabilization of the polar metal phase, but an experimental viewpoint that takes both broken symmetries and core-level specificity into account is lacking. The most common probe of broken inversion symmetry is optical second harmonic generation (SHG) spectroscopy, which has been applied previously to examine the nature of Os−O bonding in LiOsO3. However, not only is optical SHG non-element-specific, but a partial density of states (DOS) analysis reveals overwhelming contributions of Os 5d and O 2p character around the Fermi level (Figure 1c and Section 6 in the Supporting Information (SI)). In LiOsO3, the features of interest are Li−O acentric displacements. Given the orbital character of states around the Fermi surface, it is not surprising then that an order-of-magnitude weaker optical SHG signal was found in LiOsO3, compared to LiTaO3 and LiNbO3.

To gain insight into the nature of the polar phase, we turn to extreme ultraviolet second harmonic generation (XUV-SHG) spectroscopy, which is a newly developed method viable for studying bulk-phase noncentrosymmetric materials, surfaces, and buried interfaces in the XUV or the soft X-ray (SRX) regimes, where the objective is to perform SHG under resonant conditions, and in the hard X-ray regime, where a nonresonant approach is usually taken. In SRX- or XUV-SHG spectroscopy, the incident X-ray beam is resonant or half-resonant with a core-to-valence transition, such that the resulting resonantly enhanced, background-free signal is sensitive to core levels in the electronic structure. By energetically resolving the SHG emission, the symmetry breaking can be correlated to particular spectral features. The application of XUV-SHG spectroscopy to such short wave-
lengths requires the use of XUV photon sources capable of achieving high pulse intensities to drive the nonlinear light-matter response, for which X-ray free electron lasers (XFEL) are uniquely well-suited. The inherent intensity fluctuations of XFEL sources measure on a shot-to-shot basis enable measuring the nonlinear response via

\[ I(2\omega) \propto |\chi_{\text{eff}}^{(2)}(2\omega; \omega + \omega)|^2 I(\omega)^2 \]  

where \( \chi_{\text{eff}}^{(2)} \) is the effective nonlinear susceptibility, dependent on crystal cut and experimental geometry, the incident beam is at a frequency-dependent intensity, \( I(\omega) \), and SHG emission occurs with a frequency of \( 2\omega \). Here, the dielectric environment around Li in LiOsO\(_3\) below \( T_c \) is probed by tuning the incident XFEL photon energy to be half-resonant with energies around the Li K-edge at \(-56.6\) eV (Figure 1c) with contributions from nearby Os semicore states. The energy-dependent \( \chi_{\text{eff}}^{(2)} \) is extracted according to eq 1 and \( ab\) initio density functional perturbation theory (DFPT) simulations are used to relate the nonlinear response to the broken inversion symmetry. We find that the resultant nonlinear susceptibility suggests sensitivity to Li atomic displacements in the unit cell, but a lack of OsO\(_6\) octahedral rotations. Further, our results pave the way toward time- and temperature-dependent measurements of inversion symmetry-broken systems with core-level specificity.

**EXPERIMENTAL RESULTS**

XUV-SHG spectroscopy was performed on samples of LiOsO\(_3\) in its polar metal phase at \( T = 62 \) K and in its high-temperature centrosymmetric phase at \( T = 160 \) K at the BL1 beamline of the SPring-8 Angstrom Compact Free Electron Laser (SACLA). A 30 fs p-polarized XUV beam was incident at 45°, with respect to the surface normal onto the [120] plane of LiOsO\(_3\). By tuning the incident photon energy to energies ranging from 28 eV to 33 eV, the incident photon was half-resonant with the Li 1s (\(-56.6\) eV) level and close-by Os 4f (\(-61.6\) eV) and 5p (\(-60.2\) eV) levels, thus requiring two incident photons to access the valence states (Figure 1c). XUV-SHG spectra were collected by energy-dispersing the outgoing beam with a grating to simultaneously observe the fundamental and second harmonic beams using an imaging spectrometer (Figures 1d-e). Through nonlinear effects, a p-polarized fundamental photon can result in a nontrivial weighting of both s- and p-polarized frequency-doubled photons. An estimation of the relative contribution of both channels is provided in Supplementary Section S1 in the SI, but further polarization analysis is beyond the scope of this work, since the two polarizations are not experimentally resolved. The \( \chi_{\text{eff}}^{(2)} \) spectrum was then extracted using eq 1 after binning and averaging spectra based on the photon energy and intensity of the driving fundamental pulse. The inherent jitter of the XFEL, both in frequency and intensity, allowed for a high-fidelity extraction of \( \chi_{\text{eff}}^{(2)}(2\omega) \) with significantly more data points, compared to refs 21–24. For the \( T = 62 \) K set of measurements, a quadratic function was fit to a plot of \( I(\omega) \) vs \( I(2\omega) \), at each energy where the second-order fit coefficient is modulo \( |\chi_{\text{eff}}^{(2)}(2\omega)|^2 \), with \( \chi_{\text{eff}}^{(2)}(2\omega) \) a rank-three tensor of four independent components (\( \chi_{\text{xxz}}^{(2)}, \chi_{\text{yyz}}^{(2)}, \chi_{\text{zzz}}^{(2)} \), and \( \chi_{\text{xyy}}^{(2)} \)), because of point group symmetry (Figure 2e). For the measurements at 160 K, no SHG signal was discernible above the background noise, in accordance with the centrosymmetry of the LiOsO\(_3\) high-temperature phase. The lack of observable SHG above \( T_c \) further serves to rule out that the SHG from the low-temperature phase comes from broken inversion symmetry at the surface or harmonic contamination in the FEL beam.

To relate the measured nonlinear susceptibility to unit cell structure, a tensor analysis considering the experimental geometry and crystal cut was performed to arrive at a mathematical expression for \( \chi_{\text{eff}}^{(2)} \). Further details of the

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**Figure 2.** The energy-dependent nonlinear susceptibility across the Li K-edge. (a–d) \( \chi_{\text{eff}}^{(2)}(2\omega; \omega + \omega) \) and \( \chi_{\text{eff}}^{(2)} \) across the Li K-edge. (e) The energy-dependent nonlinear susceptibility shown (black points) overlaid onto the calculated \( \chi_{\text{eff}}^{(2)}(2\omega) \). For panels (a–d), the dashed gray line at \( 56.6 \) eV corresponds to the onset of the Li K-edge: darker green corresponds to larger Li displacement along the polar axis (\( d \)) of the LiOsO\(_3\) polar phase as indicated by the inset in panel (e) and in the corresponding legend. Vertical error bars correspond to errors in the quadratic fit of eq 1, whereas horizontal error bars are a result of energy jitter of the FEL.
experimental setup, data analysis, and sample preparation are described in sections S0–S4 in the SI.

According to the selection rules for SHG, electrons residing in Li 1s core states can transition to valence states of Os 5d character, whereas the Os 5p and Os 4f semicore states can transition to valence states of O 2p character (Figure 1c). The approximately 2 eV-wide gap in the DOS above the Fermi level ($E_F$) has been previously assigned to the crystal-field splitting in Os 5d-like orbitals, but the nonzero DOS directly at $E_F$ is consistent with the metallic character of LiOsO$_3$.[16]

To gain insight into how the measured spectra relate to the Li coordination environment, theoretical calculations of the LiOsO$_3$ linear absorption were performed using the exciting full-potential all-electron-extended linearized plane wave software package based on first-principles density function theory (DFT).[29] Two LiOsO$_3$ periodic cell structures, corresponding to the nonpolar and polar phases, were used. The Brillouin zone was sampled with a $15 \times 15 \times 15$ $\Gamma$-point centered $k$-point grid with the local density approximation functional.[30] DFPT simulations within the random phase approximation were used to access excited states of the system. The formalism outlined by Sharma et al., as implemented within exciting, was used to calculate the four active $\chi^{(2)}$ tensor elements (see Figures 2a–d), with the aforementioned $k$-point grid set.[31] 120 empty states were included in the ground-state calculation to account for the excited state at double the energy of the Li 1s core state. The background signal, which is the response from the valence electrons and is proportional to the inverse of energy ($\sim 1/\text{energy}$), was subtracted to obtain the effective susceptibility from the core state. The $\chi^{(2)}$ was next calculated as a function of varying Li position along the polar axis, $\alpha$, and compared to the experimental results (Figure 2e).

Simulations with OsO$_6$ displacements were also performed (see Section S9 in the SI) showing only little effect on the resulting XUV-SHG spectra. In addition, the core-level nonlinear susceptibility (see Section S8 in the SI), was calculated with the exclusion of Li 1s states (see Section S7 in the SI), the results of which suggest that the nonlinear response within the energy range probe is predominantly due to the transition from Li 1s core states to states above the Fermi level. Finally, the DFT calculations were repeated using the Vienna ab initio software package (VASP)[32], using a projector augmented wave (PAW) approach and a plane wave basis set of up to 400 eV to visualize the Kohn–Sham equation-generated charge densities within the LiOsO$_3$ unit cell. Shown in Figure 3 are projections of this charge density surface onto the [110] plane through the middle of the hexagonal unit cell.

## DISCUSSION

Absolute values of $\chi^{(2)}$ in the XUV are predicted to be on the order of 10 pm/V, which is in accordance with measured nonlinear susceptibilities of LiOsO$_3$ and chemically similar LiTaO$_3$ and LiNbO$_3$ in the optical regime.[20,33] The experimentally determined $\chi^{(2)}$ shown in Figure 2e has several features to point out. DFT calculations in which the Li 1s states are removed from the simulation basis set indicate that the XUV-SHG signal in the 56–59 eV range is a result of transitions from Li 1s states (see Figure S7.1 in the SI). This is supported by the observation in Figure 2e that the spectral feature centered at 58 eV is highly sensitive to Li atom position within the unit cell. The increase in SHG signal measured experimentally suggests that XUV-SHG is sensitive to Li atomic displacements with core-level specificity. Furthermore, DFT simulations involving OsO$_6$ octahedral rotations indicate that such motions have a very minimal affect the core-level $\chi^{(2)}$ spectrum (Figure S9.1). This observation, combined with the decreasing SHG response in the energy range above 60 eV corresponding to electronic transitions from Os semicore to O 2p states, suggests that inversion symmetry is largely maintained around the Os atoms.

Next, we turn to an analysis of how the XUV-SHG spectrum varies as a function of Li displacement $\alpha$. The main feature at 58 eV increases in magnitude with asymmetry in the Li–O dipoles along the polar axis, resulting from one of two possible factors: (a) the mere increase in the asymmetric distortion enhances the XUV-SHG signal, or (b) as Li ions are displaced toward OsO$_6$ octahedra, the aforementioned Li–O “long bonds” get shorter, leading to increased hybridization between orbitals of Li 2s and Os 2p character. This, in turn, gives more s-character to O 2p orbitals, thus opening up more selection-rule-allowed states for Li 1s electrons to transition into. The latter possibility is supported by DFT simulations since increased hybridization should lead to a downward shift in energy and a change in the density of states, which is observed in the appearance of a changing peak shape and a spectral shoulder at 57.5 eV as $\alpha$ increases.

To gain further insight into the inversion symmetry-breaking process, projections of the calculated charge density surface onto the [110] plane of the real space unit cell were examined. Shown in Figure 3 are slices of the charge density surfaces cut along the [110] plane in both the polar and nonpolar phases of LiOsO$_3$. It is immediately apparent that the polar phase is characterized by broken inversion symmetry around the Li ions, as evidenced by the unequal relative displacements of each of the Li atoms to the central Os atom in the polar phase.

The plots in Figure 3 provide further qualitative physical intuition behind spectral features of the tensor elements shown in Figures 2a–d. Here, it should be noted that the $i$th index in $\chi^{(2)}_{ijk}$ corresponds to the Cartesian direction along which dipole oscillations are generated at a frequency of $2\omega$ by driving electric fields along the $j$th and $k$th directions. The broad feature at 58 eV observed in the calculated spectra for $\chi^{(2)}_{zzz}$ and $\chi^{(2)}_{zxx}$ can be attributed to the polar displacement of Li atoms along the z-axis as the primary contributor to the broken inversion symmetry in LiOsO$_3$. It can also be seen that $\chi^{(2)}_{zxx}$ and $\chi^{(2)}_{zzz}$ increase in magnitude, but with a relatively unchanged spectral
shape as $\alpha$ increases. In contrast, $\chi^{(2)}_{xxx}$ exhibits a nontrivial $\alpha$-dependence. These observations can be contextualized by comparing the nonpolar and polar charge densities in Figure 3. Here, it is apparent that driving with a fundamental pulse along the $z$-direction will increase the asymmetry along the polar axis. Increasing $\alpha$ merely increases the amplitude of these oscillations. On the other hand, an incident laser beam polarized along the $x$-direction will alter the electron density with respect to the already present Li displacement in a complex way. Lastly, it is of note that $\chi^{(2)}_{xxx}$ changes minimally with $\alpha$. This can again be explained by the observation that there are minimal polar displacements within the $x-y$ plane for all atomic environments within the unit cell.

In summary, it is shown that XUV-SHG can selectively probe inversion-breaking symmetry in a bulk material with core-level specificity. Compared to optical SHG methods, XUV-SHG spectroscopy fills a key gap for studying structural asymmetries when the structural distortion is energetically separated from the Fermi surface and for probing symmetry-breaking in the spectral features of interest. For example, optical SHG would primarily probe Os–O acentric displacements, which obscures the Li–O acentric displacements that are the physics of interest. In addition, XUV-SHG offers the ability to access information on light atoms in a heavy-atom environment by making use of core-level resonances. A comparison of calculated charge density plots and theoretical simulations of the way the nonlinear susceptibility tensor elements vary as a function of Li displacement provide a qualitative picture for how microscopic asymmetries on unit cell length scales determine the nonlinear response. Open questions for future investigation are highlighted in three recent works. Shan et al.35 observed SHG due to electric quadrupolar effects above the polar ordering temperature up to 230 K, as a result of an extended critical fluctuation region. Such effects were not visible in XUV-SHG at 160 K, but may have been below the detection limit of this experiment. Through complementary theory calculations, Helk et al.23 noted that resonant and nonresonant contributions to SHG can be of the same order of magnitude in the XUV regime, because of allowed transitions from the valence band to high-energy continuum states. Further development of SHG methodology in the XUV and SXR regimes will be essential to deconvolute these contributions and to fully characterize element-specific responses. Lastly, we have recently demonstrated polarization-resolved XUV-SHG35 as a viable method to extract symmetry information from angle-resolved SHG responses with core-level specificity. Such a tool will add invaluable insight into systems like LiOsO$_3$ where symmetry-arguments and angular anisotropies are central to structure–function relationships. We point out that the future of XUV-SHG spectroscopy lies in its potential to track the nonlinear response as a function of both temperature and time. The sensitivity to Li atom displacement above and below $T_c$ demonstrated here highlight the viability for XUV-SHG for studying critical fluctuations, phase transitions, and interface physics in other condensed matter systems.

**ASSOCIATED CONTENT**

1 Supporting Information

The Supporting Information is available free of charge at https://pubs.acs.org/doi/10.1021/acs.nanolett.1c01502.
Walter S. Drisdell — Chemical Sciences Division and Joint Center for Artificial Photosynthesis, Lawrence Berkeley National Laboratory, Berkeley, California 94720, United States; orcid.org/0000-0002-8693-4562

Iwao Matsuda — Institute for Solid State Physics, The University of Tokyo, Kashiwa, Chiba 277-8581, Japan; Trans-scale Quantum Science Institute, The University of Tokyo, Bunkyo-ku, Tokyo 113-0033, Japan

John W. Freeland — X-ray Science Division, Argonne National Laboratory, Argonne, Illinois 60439, United States

Todd A. Pascal — ATLAS Materials Science Laboratory, Department of Nano Engineering and Chemical Engineering, Materials Science and Engineering, and Sustainable Power and Energy Center, University of California—San Diego, La Jolla, California 92023, United States

Complete contact information is available at: https://pubs.acs.org/10.1021/acs.nanolett.1c01502

Author Contributions
A.A., P.M., Y.H., IM, Y.K., S.O., KT, M.Y., C.P.S., W.S.D., and J.W.F. performed the experiments at the SACLA free-electron laser. E.B., C.B.U., and M.Z. analyzed and interpreted the experimental data. C. Wang and Y.S. synthesized the samples. H.P. and V.G. prepared and precharacterized the samples. S.J. and T.A.P. performed the simulations. W.S.D., A.A., and M.Z. performed linear reflectivity measurements at the Advanced Light Source. C. Woodahl and C.B.U. analyzed the linear reflectivity data. M.Z., C.P.S., J.W.F., and W.S.D. conceived the experiment. M.Z. supervised the project. E.B. wrote the manuscript, under the supervision of M.Z. and with input from all authors.

Notes
The authors declare no competing financial interest.

ACKNOWLEDGMENTS
M.Z., C.P.S. and A.A. acknowledge support by the Max Planck Society (Max Planck Research Group). M.Z. acknowledges support by the Federal Ministry of Education and Research (BMBF), under “Make our Planet Great Again - German Research Initiative” (Grant No. 57427209 “QUESTforENERGY”) implemented by DAAD. J.W.F., H.P. and V.G. acknowledge Department of Energy Grant No. DE-SC-0012375. W.S.D. acknowledges support from the Joint Center for Artificial Photosynthesis, a DOE Energy Innovation Hub, supported through the Office of Science of the U.S. Department of Energy, under Award No. DE-SC0004993. Measurements were performed at BL1 of SACLA with the approval of the Japan Synchrotron Radiation Research Institute (JASRI) (Proposal No. 2019B8066). This work was supported by the SACLA Basic Development Program 2018–2020. The authors would like to acknowledge the supporting members of the SACLA facility. Additional measurements were performed at beamline 6.3.2 of the Advanced Light Source, a U.S. DOE Office of Science User Facility (under Contract No. DE-AC02-05CH11231). This research used resources of the National Energy Research Scientific Computing Center, a DOE Office of Science User Facility supported by the Office of Science of the U.S. Department of Energy, under Contract No. DE-AC02-05CH11231. This work also used the Extreme Science and Engineering Discovery Environment (XSEDE), which is supported by National Science Foundation (Grant No. ACI-1548562). C. Wang and Y.S. acknowledge the National Natural Science Foundation of China (No. U2032204) and the Strategic Priority Research Program (B) of the Chinese Academy of Sciences (No. XDB33000000). C. Woodahl acknowledges support by the National Science Foundation REU Program (Grant No. 1852537). M.Z. acknowledges funding by the W. M. Keck Foundation, funding from the UC Office of the President within the Multicampus Research Programs and Initiatives (M21PL3263), and funding from Laboratory Directed Research and Development Program at Berkeley Lab (107573). We are grateful for input and discussion with David Atwood and Ramamoorthy Ramesh.

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