Aiming at solving the problem of low accuracy in traditional distance vector-hop (DV-hop) algorithm used for wireless sensor networks node location, two refined localization algorithms, that is, hyperbolic-DV-hop localization algorithm and improved weighted centroid DV-hop localization algorithm (IWC-DV-hop), are proposed in this paper. Instead of taking the average HopSize of BeaconNode nearest to the UnknownNode, hyperbolic-DV-hop algorithm chooses the average of average HopSizes of all BeaconNodes, as the average HopSize of the UnknownNode. The ML localization algorithm is also replaced by hyperbolic location algorithm. IWC-DV-hop algorithm improves the accuracy by selecting appropriate BeaconNodes and replacing ML localization with centroid localization. And a weighted scheme is used in IWC-DV-hop so that the influence of different anchors is taken into consideration. Simulations have been conducted to prove that the accuracy is improved by both of the two algorithms and IWC-DV-hop is the best choice.

1. Introduction
Wireless sensor network (WSN) is an increasingly important technology attracting considerable research interest. WSNs consist of thousands of nodes with built-in sensors which can collect a variety of information from surrounding environment. Localization is one of the most important problems in WSNs, for position information is needed in all kinds of situations [1]. In environmental monitoring applications such as bush fire surveillance, water quality monitoring, and precision agriculture, the measurement data are meaningless without knowing the location from where the data are obtained. Moreover, location estimation may enable a myriad of applications such as inventory management, intrusion detection, road traffic monitoring, health monitoring, reconnaissance, and surveillance. Sensor network localization algorithms estimate the locations of sensors with initially unknown location information by using knowledge of the absolute positions of a few sensors and intersensor measurements such as distance and bearing measurements [2]. GPS is widely used for localization, but it is impossible for WSNs to be used considering the cost limitation. So we need some special localization algorithm for WSNs.

Currently, there are many kinds of self-localization algorithms [3], which can be divided into two categories, that is, range-based and range-free [4].

Range-based algorithms use absolute point-to-point distance or angle information to calculate distance between neighbouring sensors [5]. Although the use of range measurements results in a fine-grained localization scheme, range-based algorithms require the sensor to contain additional hardware to make range measurements. There are many common range-based localization algorithms such as received signal strength indicator (RSSI) [6], time of arrival (TOA) [7], time difference of arrival (TDOA) [8], and angle of arrival (AOA) [9].

Range-free algorithms do not need absolute range information. The accuracy is much lower than the range-based but it can still satisfy many applications’ requirements. Hardware requirement of range-free algorithms is little; it does not need actual measurements of physical properties like radio signal
strengths, angle of arrival of signal, and distance, so the range-free algorithms are more economical, cost-effective, and feasible for the large-scale wireless sensor networks. There are many range-free localization algorithms, such as centroid algorithm [10], DV-hop [11, 12], amorphous [13], APIT [14], and MDS-MAP [15, 16].

WSN devices have a hardware limitation that is why solutions of range-free localization are being pursued as a cost-effective method compared to other more expensive range-based approaches [17]. In this paper we focus on DV-hop, one of the range-free localization algorithms.

Extensive research has been done on the application of DV-hop algorithm since the algorithm was first proposed by Niculescu and Nath in 2001 [6, 7]. It is still very popular due to its simplicity, cost-effectiveness, and robustness. Therefore researchers keep working on its improvement.

In [18], Dulman and Havinga discussed the influence of the underlying random topology, and based on that they derived a distance estimation function of the hop count by which two nodes are separated and characterized the precision of these estimations. And they obtained the improvement of roughly 26% for DV-hop localization algorithm in position accuracy.

Checkout DV-hop algorithm and selective 3-anchor DV-hop algorithm were proposed by Gui et al. A calculation step, called checkout step, was added to DV-hop in checkout DV-hop [19]. In selective 3-anchor DV-hop algorithm, the normal node first selects any three anchors to form a 3-anchor group; then it calculates the candidate position based on each 3-anchor group, and finally according to the relation between candidate positions and the minimum hop counts to anchors, the normal node chooses the best candidate position [20].

DV-hop + Lastdist algorithm was proposed by Zhang et al. in [21]. A distance variable of final hop was added to the DV-hop communication message. The distance from the node to the anchor node can properly reduce the error distance caused by the final hop.

WD-DV-hop was proposed by Lin et al. in [22]. The centralized and distributed calculation method is replaced by a weighted calculation method. The distance between unknown nodes and anchor nodes is calculated by a method, in which the average one-hop distance of each anchor node multiplies by hops count between unknown nodes and anchor node.

There are also some researchers working on centroid localization algorithm. In [23] Deng et al. applied his improved centroid localization algorithm in WSN. He proposed a centroid algorithm with selected anchor node localization algorithm (SA-Centroid) for WSNs. The triangle centroid and polygon centroid were used and the method of selecting nearest anchor node was adopted. However, the SA-Centroid is complex and the amount of calculation is huge. Furthermore the accuracy improvement is limited. Based on the related work above, we proposed our DV-hop algorithm, which is simpler and provides better localization accuracy.

The rest of this paper is organized as follows. In Section 2, we briefly review two other researchers’ study on DV-hop’s improvement which we have realized. In Section 3, original DV-hop localization algorithm is briefly introduced. In Section 4, we introduce how we refine DV-hop, and the simulation results are illustrated in Section 5. We also compare and analyze the difference between original DV-hop and our two algorithms, as well as the difference between our two algorithms and other improved DV-hop algorithms. Finally, we present our conclusions in Section 6.

2. Related Works

In [24], Li et al. proposed an improved DV-hop algorithm, named weighted DV-hop algorithm (WDV-hop). Jian Li’s algorithm is derived from DV-hop algorithm and uses weight of anchors to improve localization accuracy without any additional hardware device. Jian Li’s algorithm gives every anchor a weight which reflects the effects of anchor. In Jian Li’s algorithm an unknown node computes the hop-size based on all the hop-size values it receives from the anchors, instead of just taking the first received hop-size value as in original DV-hop algorithm. Using this strategy, the position of unknown nodes is calculated by using weighted least square method.

In [25], Zhang et al. analyse the drawback of DV-hop and centroid location algorithm and proposed a new weighted centroid algorithm based on DV-hop, named weighted centroid localization algorithm (WCL). Their algorithm uses weight of anchors to improve accuracy. Every anchor node is weighted by a value reflecting the effect of the anchor node on the unknown node.

We have realized these two algorithms by programming with MATLAB so that we can compare our proposed algorithms with them from lots of aspects. The comparison and analysis will be made after we introduce our algorithms in following sections.

3. Theoretical Background

In this paper, we focus on static networks, where nodes do not move, since this is already a challenging condition for distributed localization. We assume that some anchor nodes, named BeaconNode, have a priori knowledge of their own positions. Note that anchor nodes have the same capabilities (processing, communication, energy consumption, etc.) as all other sensor nodes with unknown positions, which are named UnknownNode.

3.1. DV-Hop Localization Algorithm. The traditional DV-hop algorithm was developed by Niculescu and Nath [6, 7]. It can be summarized as in the following three steps.

3.1.1. Finding the Minimum HopCount. In the first step, all BeaconNodes broadcast beacon messages to other nodes; the format of the beacon message is \{id, x, y, HopCount\}. The initial value of HopCount is 0. Each receiving node maintains a BeaconNode information table and keeps the minimum HopCount value from other nodes. After a period of time, all nodes in the network will have the minimum HopCount to other nodes.
3.1.2. Calculation of the Distance between BeaconNodes and UnknownNodes. In the second step, the BeaconNodes get minimum HopCount value to other BeaconNodes according to the result in the first step. Then it can estimate average HopSize to other BeaconNodes on the basis of the minimum HopCount and the distance between BeaconNodes. The HopSize to other BeaconNodes on the basis of the minimum HopCount is obtained by

\[
\text{HopSize}_i = \frac{\sum_{j=1,j\neq i}^{N} h_{ij}}{\sum_{j=1,j\neq i}^{N} h_{ij}},
\]

(1)

where \((x_i, y_i)\) and \((x_j, y_j)\) are coordinates of BeaconNodes \(i\) and \(j\), \(h_{ij}\) is the minimum HopCount value between BeaconNodes \(i\) and \(j\). \(N\) presents the quantity of BeaconNodes. Every BeaconNode broadcasts its average HopSize to the whole network. Each UnknownNode receives all BeaconNodes' average HopSize and selects the HopSize of a BeaconNode, which has the minimum HopCount value to this UnknownNode, as its average HopSize. In the end, we can calculate the distance of every UnknownNode to BeaconNode by

\[
d_{ij} = \text{HopSize}_i \times \text{HopCount}_{ij},
\]

(2)

where \(d_{ij}\) is the distance between the \(i\)th UnknownNode and \(j\)th BeaconNode. \(\text{HopCount}_{ij}\) indicates the minimum HopCount between the \(i\)th UnknownNode and \(j\)th BeaconNode.

3.1.3. Calculation of Estimated Location. In the third step, the UnknownNode can calculate their locations by maximum likelihood (ML) estimation [26] or trilateration. In this paper we choose ML estimation and it will be introduced in the next section.

3.2. Maximum Likelihood Estimation. ML estimation is a good way to calculate UnknownNodes' locations [4, 5, 27, 28]. With its help, we can obtain the following set of equations:

\[
\sqrt{(x_i - x_1)^2 + (y_i - y_1)^2} = d_{11},
\]

\[
\sqrt{(x_i - x_2)^2 + (y_i - y_2)^2} = d_{12},
\]

\[
\vdots
\]

\[
\sqrt{(x_i - x_N)^2 + (y_i - y_N)^2} = d_{1N},
\]

(3)

where \(d_{ij}\) represents the distance of \(i\)th UnknownNode to the first BeaconNode, \(N\) presents the quantity of BeaconNode, \((x_1, y_1), (x_2, y_2), \ldots, (x_N, y_N)\) are the coordinates of BeaconNode. Then (3) can be transformed by

\[
AX = B,
\]

(4)

where \(A\) is

\[
\begin{bmatrix}
x_1 - x_N & y_1 - y_N \\
x_2 - x_N & y_2 - y_N \\
\vdots & \vdots \\
x_{N-1} - x_N & y_{N-1} - y_N
\end{bmatrix},
\]

(5)

\[X\]

is

\[
\begin{bmatrix}
x_i \\
y_i
\end{bmatrix},
\]

(6)

and \(B\) is

\[
\begin{bmatrix}
x_1^2 - x_N^2 + y_1^2 - y_N^2 - d_{11}^2 + d_{1N}^2 \\
x_2^2 - x_N^2 + y_2^2 - y_N^2 - d_{1N}^2 + d_{2N}^2 \\
\vdots \\
x_{N-1}^2 - x_N^2 + y_{N-1}^2 - y_N^2 - d_{(N-1)N}^2 + d_{NN}^2
\end{bmatrix}.
\]

(7)

According to the least square method, the solution of (4) should be

\[
\hat{X} = (A^TA)^{-1}A^TB.
\]

(8)

3.3. Centroid Localization Algorithm. This section is devoted to the centroid algorithm. It is the most basic schemes, and it comprises three stages. First, BeaconNodes broadcast the localization reference to its neighbourhoods. In the second stage, the UnknownNodes receive and restore the information transmitted by at least three different BeaconNodes and then, classical arithmetic mean is employed to calculate the position of UnknownNode. Each UnknownNode maintains a table \{beacon's id, position of the beacon \((x, y)\)\}. In stage 3, when obtaining its coordinate, the UnknownNode becomes a BeaconNode that propagates packets to its vicinity.

Figure 1 shows the detailed interpretation of the centroid algorithm. In centroid algorithm based positioning, the UnknownNode's estimation coordinate is the centroid of the polygon formed by BeaconNodes. Suppose that there are five BeaconNodes around the UnknownNodes \(A_1(x_1, y_1), A_2(x_2, y_2), A_3(x_3, y_3), A_4(x_4, y_4),\) and \(A_5(x_5, y_5)\) distributed around the UnknownNode \((S(x, y))\). Thus the position of UnknownNode \(S\) can be calculated using:

\[
(x, y) = \left(\frac{x_1 + x_2 + x_3 + x_4 + x_5}{5}, \frac{y_1 + y_2 + y_3 + y_4 + y_5}{5}\right).
\]

(9)

The general algorithm can be summarized using (10), where \(N\) presents the quantity of BeaconNode:

\[
x_{\text{est}} = \frac{\sum_{i=1}^{N} x_i}{N}, \quad y_{\text{est}} = \frac{\sum_{i=1}^{N} y_i}{N}.
\]

(10)

4. Improvement of DV-Hop

Localization Algorithm

In this section, we present two enhanced DV-hop algorithms, that is, hyperbolic-DV-hop localization algorithm
and IWC-DV-hop localization algorithm. The original DV-hop takes the average HopSize of BeaconNode nearest to the UnknownNode, which is believed to be the reason leading to large errors. So we replace it with the average of average HopSizes of all BeaconNodes, as the average HopSize of the UnknownNode. The ML localization algorithm is replaced by Hyperbolic location algorithm, which has better performance results. In IWC-DV-hop algorithm, centroid algorithm is combined with DV-hop algorithm, and a weighted scheme is used in IWC-DV-hop so that the influence of different anchors is taken into consideration.

**4.1. Our Hyperbolic-DV-Hop Localization Algorithm.** After a thorough study of the principle of original DV-hop localization algorithm, we found that the errors of original DV-hop localization algorithm are caused by HopCounts, averaging HopSizes, and localization algorithm. So we managed to improve it through working on the last two steps, that is, the way to calculate distance between BeaconNode and UnknownNode and the localization algorithm.

4.1.1. Refinement on Second Step—Distance Estimation. As what we have introduced above, UnknownNodes, in original DV-hop algorithm, take the average HopSize of its nearest BeaconNode as their own average HopSize. But the nodes in the WSN are disposed stochastically, which means the path between nodes may be not straight, which is the reason why the average HopSizes are always bigger than the actual value.

When the distance between UnknownNode and BeaconNode is calculated using the average HopSize, the error is always large. The nearest BeaconNode is unique and cannot be used to represent the whole BeaconNodes. Since ML in the third step will make use of the distance between UnknownNodes and every BeaconNode, it is a good way to take the average HopSize of all BeaconNodes to replace that of the nearest BeaconNode for UnknownNodes.

We calculate the average HopSizes of all BeaconNodes by

\[
\text{HopSize}_{\text{avg}} = \frac{\sum_{i \neq j} (x_i - x_j)^2 + (y_i - y_j)^2}{\sum_{i \neq j} h_{ij}},
\]

where \((x_i, y_i)\) and \((x_j, y_j)\) are coordinates of BeaconNodes \(i\) and \(j\) and \(h_{ij}\) is the minimum HopCount value between BeaconNodes \(i\) and \(j\). Then we can calculate the average of the average HopSize of BeaconNodes and take this as the average HopSize of every UnknownNode—HopSize\(_{\text{UN}}\):

\[
\text{HopSize}_{\text{UN}} = \text{HopSize}_{\text{avg}} = \frac{\sum \text{HopSize}_{ij}}{n}.
\]

4.1.2. Refinement on Third Step—Location Algorithm. In the original DV-hop algorithm, ML or trilateration is used for physical distances estimations. In this paper, we use hyperbolic location algorithm [29, 30] to replace ML.

We derive the following expression:

\[
X_N^2 + Y_N^2 - 2X_N X_i - 2Y_N Y_i + X_i^2 + Y_i^2 = d_{iN}^2
\]

\[
\implies d_{iN}^2 - E_N = -2X_N X_i - 2Y_N Y_i + K,
\]

where \(E_N = X_N^2 + Y_N^2\) and \(K = X_i^2 + Y_i^2\). Set

\[
P_c = [X_i, Y_i, K]^T,
\]

\[
M_c = \begin{bmatrix}
-2X_1 & -2Y_1 & 1 \\
-2X_2 & -2Y_2 & 1 \\
\vdots & \vdots & \vdots \\
-2X_N & -2Y_N & 1
\end{bmatrix},
\]

\[
h_c = \begin{bmatrix}
d_1^2 - E_1 \\
d_2^2 - E_2 \\
\vdots \\
d_N^2 - E_N
\end{bmatrix}.
\]

We can derive from (8) that

\[
M_c S_c = h_c.
\]

Using the least square algorithm [30], from (14), we can get

\[
P_c = (M_c^T M_c)^{-1} M_c^T h_c.
\]

Then, the position of \(i\) th UnknownNode should be

\[
(P_c (1), P_c (2)).
\]

4.2. Our Improved Weighted Centroid DV-Hop Localization Algorithm. The accuracy improvement of Hyperbolic-DV-hop localization algorithm is still limited, so we have further proposed our improved weighted centroid DV-hop localization algorithm. Firstly, we simply replace the hyperbolic algorithm with centroid algorithm. Secondly, we analyse the reason leading to errors and then offer our solutions which turn out to improve the accuracy.
4.2.1. Refinement on the Third Step—Using Centroid Algorithm to Calculate the Unknown Nodes’ Location. In the second step in original DV-hop algorithm, we can get the distance, \( d_{ij} \), between BeaconNodes and UnknownNodes via (2). The UnknownNodes receive and restore the information transmitted by at least three different BeaconNodes. Then we set a threshold distance and all the BeaconNodes with the distance between them and the UnknownNode less than the threshold distance will be selected. At last, the centroid of all the selected BeaconNodes is calculated and is taken as the UnknownNode’s estimated location [31]. Suppose there are BeaconNodes \( B_i(x_i, y_i), i = 1, 2, \ldots, n \), distributed around the UnknownNode \( UN_j(x_j, y_j) \), and the threshold distance is \( D_{\text{threshold}} \). \( D_{ij} \) represents the distance between \( B_i(x_i, y_i) \) and \( UN_j(x_j, y_j) \). The positions of the BeaconNodes whose \( D_{ij} \) is less than \( D_{\text{threshold}} \) are restored in \( B_i(x_k, y_k) \). Thus the position of UnknownNode \( UN_j(x_j, y_j) \) can be calculated using:

\[
X_j = \frac{\sum X_k}{k}, \quad Y_j = \frac{\sum Y_k}{k}.
\]

4.2.2. Further Analyses of the Reason for Error in DV-Hop. We have discussed one of the reasons why the error exists in original DV-hop in Section 4.1; that is, the original DV-hop takes the average HopSize of BeaconNode nearest to the UnknownNode. We replace it with the average of average HopSizes of all BeaconNodes, as the average HopSize of the UnknownNode. But the improvement of accuracy is limited. After further analysing the DV-hop algorithm, we found that error can be further reduced by adopting a new method.

In the second step of the original DV-hop, UnknownNode uses (2) to calculate the distance between itself and BeaconNodes. The distance can also be calculated by multiplying BeaconNodes’ HopSize by HopCount from another perspective. In other words, the HopSize of UnknownNodes is not necessary anymore. That means we can cut out one little step from the second step of DV-hop.

4.2.3. Refinement on the Second Step of DV-Hop. The HopSize of UnknownNode is not needed anymore and the step to calculate the HopSize of UnknownNode is cut out. The HopSize, can be replaced by HopSize, and then the distance between UnknownNode \( UN_i \) and BeaconNode \( j \) can be obtained by

\[
d_{ij} = \text{HopSize}_j \ast \text{HopCount}_{ij}.
\]

Since we have known the HopSize of every BeaconNode and the HopCount between every node and every noode, it is easy to get the distance between every UnknownNode and each BeaconNode.

The accuracy will be improved since the total number of steps for localization is decreased. From mathematical point of view, the calculation result will be less accurate in the case where an estimated value is calculated (added, subtracted, multiplied, divided, etc.) for \( N + 1 \) times than the case where it is calculated for \( N \) times. So the accuracy is improved when we cut out one calculating step from original DV-hop algorithm.

4.2.4. Further Analyses of the Reason for Error in Centroid Algorithm. In the centroid algorithm, the unknown node’s estimation coordinate is the centroid of the polygon formed by BeaconNodes. And centroid algorithm cannot reflect the influence of the distance between BeaconNodes and UnknownNodes. In fact, the BeaconNodes which are closer to the UnknownNode will have a greater impact on the UnknownNode. Different BeaconNodes have different effect on the UnknownNode, considering the distance between them. But the centroid algorithm treats them as the same kind of node. In order to embody the effect of BeaconNodes which have different distance on the accuracy calculation, our improved weighted centroid DV-hop (IWC-DV-hop) algorithm is proposed.

4.2.5. Refinement on the Centroid Algorithm. As what (2) and (21) have showed, distance between BeaconNodes and UnknownNodes has a direct correlation with HopCounts. So the effect of distance on accuracy can be replaced by HopCounts. Then we can calculate the location of UnknownNodes by

\[
X_{\text{est}} = \frac{\sum_{i=1}^{n} w_i x_i}{\sum_{i=1}^{n} w_i}, \quad Y_{\text{est}} = \frac{\sum_{i=1}^{n} w_i y_i}{\sum_{i=1}^{n} w_i},
\]

where \((x_{\text{est}}, y_{\text{est}})\) is the coordinates of the UnknownNode. And we suppose it has received \( n \) BeaconNodes’ message \( ((x_1, y_1), (x_2, y_2), \ldots, (x_n, y_n)) \). \( w_i \) is the weight of BeaconNode \( i \), and its value can be obtained by

\[
w_i = \frac{\sum_{j=1}^{n} \text{hop}_j}{n \text{hop}_i},
\]

where hop\(_i\) is the HopCount between the UnknownNode and the BeaconNode \( i \). These weights determine the relative importance of each quantity on the average. Consequently, when the weight \( w_i \) is larger than the other weights, the weights \( w_i \) play a more important role on the average. This scheme ensures that the closest BeaconNode will affect the localization result mostly.

Another advantage with our improvement to the original centroid algorithm is that without threshold the weighted solution can make full use of all BeaconNodes available. While only those BeaconNodes whose \( D_{ij} \) is less than \( D_{\text{threshold}} \) are used in the original centroid algorithm. On the other hand, how to choose a perfect threshold is also a complex issue requiring more discussion, which is avoided in the weighted solution.

5. Simulation and Performance Comparison

We compare the performance of different locating methods by evaluating the average location error for each algorithm. The performance comparisons are conducted using a simulator developed with MATLAB R2013a, and all the nodes are deployed in a 500 m \( \times \) 500 m area.

The comparison with other two researchers’ algorithms has also been made in this section. We have realized their algorithms by programming according to their description in [24, 25].
5.1. Varying the Beacon Node Ratio. Firstly we compare the performance of three localization algorithms with different Beacon Node ratios. Suppose the number of all nodes is 800, and the communication radius of Beacon Node is 100 m. We calculated the average of results of 50 simulations and set the average as the error ratio. Gradually, we increased the ratio of Beacon Node and get the different results in different situations.

The performance comparison with 3 different localization algorithms is shown in Figure 2. The upper line shows the error ratio of original DV-hop algorithm varies with the increase of the Beacon Node ratio, while the middle line shows the error ratio of hyperbolic-DV-hop algorithm and the lower line shows the error ratio of our IWC-DV-hop. It is obvious to observe that our IWC-DV-hop algorithm is much superior to the other two. In fact, the accuracy improvement of our hyperbolic-DV-hop over the original DV-hop is 8.2%, while our IWC-DV-hop over the original DV-hop is 63%.

Figure 3 shows the comparison between our hyperbolic-DV-hop algorithm, our IWC-DV-hop algorithm, Jian Li’s WDV-hop algorithm in [24], and Bingjiao Zhang’s WCL algorithm in [25]. Overall, it is obvious that our IWC-DV-hop algorithm performs best with the least error ratio. We can also conclude that our proposed two algorithms are more stable, for their fluctuation range is smaller with the variety of Beacon Node ratio than that of Jian Li’s WDV-hop algorithm and Binjiao Zhang’s WCL algorithm. In addition, the environment with low density of Beacon Nodes is simulated and compared. The result shows that our IWC-DV-hop algorithm still has the best accuracy and is qualified for this kind of environment.

5.2. Varying Node Number. When we compare the performance of three localization algorithms with different nodes number, we set the Beacon Node ratio to 50% and communication radius to 100 m. We calculated the average of results from 50 simulation experiments and set the average as the error ratio. Furthermore, we increased nodes number from 300 to 800 to get the different results in different situations.

Figure 4 illustrates the contrast with three different algorithms with different nodes number. The upper line shows the error ratio of original DV-hop algorithm varies with the increase of the nodes number, while the middle line shows the error ratio of hyperbolic-DV-hop algorithm and the lower line shows the error ratio of our IWC-DV-hop. We observe that, to a certain extent, the hyperbolic algorithm improves the accuracy, while the IWC-DV-hop algorithm improves the
accuracy on a much larger scale. The accuracy improvement of our hyperbolic-DV-hop over the original DV-hop is 10.3%, while our IWC-DV-hop over the original DV-hop is 59%.

Figure 5 shows the relationship between error ratio and node number. In this simulation, we compare the accuracy of our proposed hyperbolic-DV-hop, our proposed IWC-DV-hop algorithm, Jian Li’s WDV-hop algorithm in [24], and Bingjiao Zhang’s WCL algorithm in [25]. This simulation result has proven the validity of IWC-DV-hop, since it always has the least error ratio and fluctuation.

### 5.3. Varying Communication Radius

In this scenario, we investigate the impact of increasing communication radius of BeaconNodes. The BeaconNode ratio is set as 50%, and node number is 800. We calculated the average of results of 50 simulations and set the average as the error ratio. We construct the performance comparison by artificially increasing the communication radius of BeaconNode with 10 m, and the result is plotted in Figures 6 and 7.

As what has been introduced above, the upper line shows the error ratio of original DV-hop algorithm varies with the increase of the communication radius, while the middle line shows the error ratio of hyperbolic-DV-hop algorithm and the lower line shows the error ratio of our IWC-DV-hop. We note that the accuracy is greatly improved by IWC-DV-hop, and the hyperbolic algorithm also works better than the original DV-hop. According to our records, the accuracy improvement of our hyperbolic-DV-hop over the original DV-hop is 9.3%, while our IWC-DV-hop over the original DV-hop is 62%.

Figure 7 indicates that, in general, the accuracy of our IWC-DV-hop is much better than Jian Li’s WDV-hop algorithm and Bingjiao Zhang’s WCL algorithm. It is worth mentioning that Jian Li’s algorithm has better accuracy than our hyperbolic-DV-hop algorithm when the BeaconNode communication radius is larger than 60 m, but our hyperbolic-DV-hop algorithm performs better in those environments, the communication radius is small. We can conclude that the change in BeaconNode communication radius had minimal impact on performance, which means our two proposed algorithms have better stability.

### 6. Conclusions

Localization problem is one of the most important and different problems for WSNs. After a detailed study of
positioning problem of wireless sensor network node localization, two refined distance vector-hop (DV-hop) localization algorithms, hyperbolic-DV-hop localization algorithm and IWC-DV-hop localization algorithm, are proposed in this paper. Compared to the original DV-hop algorithm, the accuracy is improved by both algorithms, between which IWC-DV-hop performs even better. Our hyperbolic-DV-hop algorithm provides better accuracy than the original DV-hop algorithm because it chooses the average of average HopSizes of all BeaconNodes as the average HopSize of the UnknownNode instead of taking the average HopSize of BeaconNode nearest to the UnknownNode. It also replaces the ML localization algorithm with hyperbolic location algorithm with better performance results. Our IWC-DV-hop algorithm improves the accuracy by selecting appropriate BeaconNodes and replacing ML localization with centroid localization. A weight scheme has also been proposed to improve the accuracy by taking the influence of different BeaconNodes into consideration. Then we run simulations to compare the performance of different localization algorithms with different parameters. The results of simulations show that both our hyperbolic-DV-hop algorithm and IWC-DV-hop are much better than DV-hop localization algorithm. In addition, comparing to other localization algorithms for WSNs or other refined algorithms based on DV-hop, our IWC-DV still performs excellently. According to our simulations, our IWC-DV algorithm not only has a much better precision but also performs much more steadily no matter how the parameters change.

In the future, we will be interested in refining our localization algorithms even further and try to use it in the 3D situations. Some test-bed can also be constructed to allow us to compare real results with those simulation results.

Conflict of Interests

The authors declare that there is no conflict of interests regarding the publication of this paper.

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