Electron transport through metal/MoS$_2$ interfaces: edge- or area-dependent process?

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Abstract

In ultra-thin two-dimensional (2-D) materials, the formation of ohmic contacts with top metallic layers is a challenging task that involves different processes than in bulk-like structures. Besides the Schottky barrier height, the transfer length of electrons between metals and 2-D monolayers is a highly relevant parameter. For MoS$_2$, both short (≤30 nm) and long (≥0.5 µm) values have been reported, corresponding to either an abrupt carrier injection at the contact edge or a more gradual transfer of electrons over a large contact area. Here we use ab initio quantum transport simulations to demonstrate that the presence of an oxide layer between a metallic contact and a MoS$_2$ monolayer, for example TiO$_2$ in case of titanium electrodes, favors an area-dependent process with a long transfer length, while a perfectly clean metal-semiconductor interface would lead to an edge process. These findings reconcile several theories that have been postulated about the physics of metal/MoS$_2$ interfaces and provide a framework to design future devices with lower contact resistances.
Transistors made of novel two-dimensional (2-D) materials beyond graphene such as single-layer MoS$_2$\textsuperscript{1} have generated considerable excitement among the scientific community for their potential as active components of future integrated circuits. Transition metal dichalcogenides (TMDs),\textsuperscript{2} black phosphorus,\textsuperscript{3,4} and hundreds of other presumably exfoliable 2-D monolayers\textsuperscript{5} appear as excellent candidates to outperform Si FinFETs, the current workhorse of the semiconductor industry, for next-generation ultra-scaled logic switches.\textsuperscript{6}

The advantages of 2-D materials over competing technologies reside in their naturally passivated surfaces, their planar geometry providing an excellent electrostatic control,\textsuperscript{7} their exceptionally high carrier mobilities as compared to 3-D compounds with the same sub-nanometer thickness,\textsuperscript{8–10} and the possibility of stacking them on top of each other to form van der Waals heterostructures.\textsuperscript{11–13}

Before MoS$_2$ field-effect transistors (FETs) with a monolayer channel can reach their full potential and deliver the expected performance,\textsuperscript{14} several key challenges remain to be solved. The source and drain contact resistances represent one of the main limiting factors as they usually lie in the k$\Omega$ · $\mu$m range,\textsuperscript{15,16} instead of 150 to 200 $\Omega$ · $\mu$m as in conventional Si transistors\textsuperscript{1}. Lower values have been reported with metalized 1T MoS$_2$\textsuperscript{17} or nickel-etched graphene\textsuperscript{18} electrodes, in the order of 200 $\Omega$ · $\mu$m, but for multilayer MoS$_2$. While top contacts are the most widely used variants due to their ease of fabrication, side contacts have started to emerge as a promising alternative,\textsuperscript{19–22} motivated by theoretical studies that predict a stronger orbital overlap and shorter tunneling distances between metals and MoS$_2$ in lateral configurations.\textsuperscript{23,24} Apart from the electrode geometry, other well-known techniques have been applied to reduce the contact resistance of MoS$_2$ FETs, among them the usage of different metals,\textsuperscript{25,26} the introduction of an interfacial layer between the metal and semiconductor,\textsuperscript{27–29} or the doping of MoS$_2$.\textsuperscript{30,31} Despite significant progresses made over

\textsuperscript{1}https://irds.ieee.org/roadmap-2017
the last few years, metal/MoS$_2$ interfaces have not yet revealed all their secrets, hindering the development of future electronic components based on 2-D materials.

An open issue of critical importance concerns the trajectories followed by electrons leaving a top metal contact and entering a MoS$_2$ monolayer situated underneath. The transfer length $L_T$, as illustrated in Fig. 1, characterizes the average distance that is needed by carriers to accomplish this transition. No consensus exists on the magnitude of $L_T$, i.e. on whether the electrical current flows through the metal up to the edge of its interface with MoS$_2$ (edge process, $L_T \simeq 0$) or whether electrons gradually penetrate into MoS$_2$ over a relatively long distance (area-dependent process, large $L_T$). In the former case, the current would
be proportional to the width $w$ of the electrode on $\text{MoS}_2$, whereas in the latter, it would also depend on the contact length $L_C$, i.e. on the length of the metal/$\text{MoS}_2$ overlap region, provided that $L_C < L_T$. Experimentally, Liu et al.\textsuperscript{32} deduced a transfer length of about 600 nm for titanium-connected single-layer $\text{MoS}_2$. Meanwhile, English et al.\textsuperscript{33} reported pure Au electrodes on top of bilayer $\text{MoS}_2$ with low contact resistances $R_C = 740 \, \Omega \cdot \mu\text{m}$ and $L_T \approx 30 \, \text{nm}$, which can be considered a near-edge process.

Obviously, these results are in total contradiction. Various modeling efforts have attempted to identify transfer mechanisms that could explain these opposite trends, but so far without much success. A prominent study relying on density functional theory (DFT), an \textit{ab initio} method, concluded that the transfer of electrons from Ti to $\text{MoS}_2$ should be area-dependent as this 2-D material gets metalized when put in contact with titanium.\textsuperscript{23} Another work combining DFT and quantum transport calculations within the framework of the Non-equilibrium Green’s Function (NEGF) formalism found that carriers preferably escape the Ti electrode at the edge of the Ti/$\text{MoS}_2$ interface.\textsuperscript{34} Finally, device simulations performed in the effective mass approximation suggested that the transfer length increases with the $\text{MoS}_2$ thickness, going from an edge process in monolayers to an area-dependent injection in multi-layer crystals.\textsuperscript{35} The apparently contradictory conclusions of these theoretical investigations do not resolve the discrepancies observed experimentally.

To address them, a deeper look at the fabrication of top contacts on 2-D materials should be taken. It has been recently shown that if titanium is deposited on $\text{MoS}_2$ under moderately high vacuum conditions ($\sim 10^{-6} \, \text{mbar}$), a TiO$_2$ oxide layer forms at the metal-semiconductor interface. Under ultra-high vacuum ($\sim 10^{-9} \, \text{mbar}$), this does not happen, allowing the Ti atoms to directly bind to the top S atoms.\textsuperscript{36} In this context, the main difference between the results of Refs.\textsuperscript{32} and \textsuperscript{33} may be the pressure at which the contacts were deposited (moderately high vs. ultra-high vacuum), not the choice of the electrode metal (Ti vs. Au) or the $\text{MoS}_2$ thickness (mono- vs. bi-layer). It is likely that an interfacial oxide layer was present within the Ti/$\text{MoS}_2$ stacks of Ref.\textsuperscript{32} but not within the Au/$\text{MoS}_2$ ones of Ref.\textsuperscript{33} The goal of
Figure 2: Schematic view of the atomic unit cells of the (a) Ti-MoS$_2$ and (b) Ti-TiO$_2$-MoS$_2$ contact geometries simulated with DFT and used to construct MLWF-based Hamiltonian matrices. The colored spheres represent individual atoms: gray - Ti, red - O, orange - Mo, and yellow - S. The right sub-plots show the corresponding band alignments. In (a), only a small portion of the unit cell is depicted as the real one contains 576 atoms, whereas in (b), the 306 considered atoms are plotted. (c) Electronic bandstructure around the Fermi level $E_f=0$ eV for the Ti-MoS$_2$ system. The primitive unit cell delimited by the dashed green rectangle in (a) served as input to this calculation. The dotted gray lines are bands lying within the Ti contacts, blue lines within MoS$_2$. A Schottky barrier height (SBH) $\Phi_{B1}=166$ meV can be extracted. (d) Same as (c), but for the Ti-TiO$_2$-MoS$_2$ unit cell in (b). The dashed red lines refer to the TiO$_2$ bands. Here, a SBH $\Phi_{B2}=293$ meV was found. The conduction band offset between MoS$_2$ and TiO$_2$ was adjusted to $\Delta_{ox}=150$ meV. Because of the different shape of the MoS$_2$ supercells in (a) and (b), the conduction band minimum of this material in (c) and (d) was not folded to the same $k$-point.

This paper is therefore to analyze the role played by such layers in the contact physics, to determine their influence on the transfer length of electrons at metal/MoS$_2$ junctions, and to find out whether they can be leveraged to reduce the contact resistance of 2-D devices. To do that, we performed $ab$ $initio$ quantum transport simulations and demonstrated that in the absence of an intercalated oxide layer between the top metal contact and MoS$_2$, the transfer of electrons becomes edge-dependent. Finally, the aforementioned results from the literature are re-examined in light of these findings.

To highlight the impact of an interfacial TiO$_2$ oxide layer on the electron transfer process, we simulated Ti-contacted single-layer MoS$_2$ structures, with and without TiO$_2$ in between, by combining plane-wave DFT, maximally localized Wannier functions (MLWFs), and NEGF. The first step consisted of creating suitable atomic geometries. Since DFT
calculations are computationally very demanding, periodic unit cells of the smallest possible
dimensions were created, while still large enough to allow for the extraction of the band-
structure and wavefunction of three distinct regions: one with pure Ti, another one made
of Ti-(TiO$_2$)-MoS$_2$, and a last one containing MoS$_2$ only. For simplicity, the underlying
substrate layer was not included in the DFT study. Atomic configurations fulfilling these
conditions are illustrated in Figs. 2(a) and (b). Next, their electronic structure was calcu-
lated with the VASP$^{38}$ DFT tool within the generalized gradient approximation (GGA) of
Perdew, Burke, and Ernzerhof.$^{39}$ The single-particle wavefunctions were then transformed
into a set of MLWFs with the help of the Wannier90$^{40}$ package.

From the chosen unit cells and the produced MLWF Hamiltonian blocks, larger struc-
tures with a $\sim$50 nm long free standing MoS$_2$ part and metal-semiconductor overlap lengths
ranging from 6 to 133 nm were constructed following the procedure described in Ref.$^{41}$ Even
though there is no region with pure Ti in Fig. 2(a) and (b), the influence of MoS$_2$ and
TiO$_2$/MoS$_2$ on Ti was found sufficiently weak such that a representative Ti Hamiltonian
block could be safely cut off from the generated heterostructures. Similarly, in Fig. 2(b), the
penetration of the metal wavefunction into the MoS$_2$ monolayer was small enough so that
the required Hamiltonian blocks of free-standing MoS$_2$ could be directly derived from the
matrix elements of the whole stack. It has been previously verified that the bandstructures
of all individual layers (Ti, TiO$_2$, and MoS$_2$), computed after the MLWF transformation and
the single block extraction, agree well with what is obtained from pure Ti, TiO$_2$, and MoS$_2$
unit cells.$^{41}$ The results are shown in Figs. 2(c) and (d).

Although DFT is considered a very accurate technique to capture both the conduction
(CB) and valence band (VB) states of semiconductors and insulators, it suffers from a well-
known band gap underestimation problem. Consequently, the calculated band alignments
may not always be reliable. Furthermore, finite size effects may take place in small simulation
domains, especially with a random placement of the constituting atoms. This issue was
avoided in our DFT calculations, which are limited in size, by replacing amorphous TiO$_2$ with
Figure 3: (a) Schematic view of the structures simulated in this work. Ti-(TiO$_2$)-MoS$_2$ systems were constructed with a pure Ti region of length $L_S = 9.5$ nm, a Ti-(TiO$_2$)-MoS$_2$ overlap region of length $5.7 \leq L_{overlap} \leq 132.8$ nm, and a MoS$_2$-only region of length $L_{semiconductor} = 47.7$ nm. Electrons are injected at the contact labeled $S$ (source) and collected at the one denoted $D$ (drain). The channel is separated from a back gate electrode by a perfectly isolating HfO$_2$ oxide layer of thickness $t_{ox} = 3$ nm and relative dielectric constant $\epsilon_R = 20$. Transport occurs in the $x$ and $y$ directions, the $z$-axis (out-of-plane) is assumed periodic. (b) Electrostatic potential energy along the vertical dashed green line in (a) at a back gate voltage $V_{gs} = 0$ (dashed line) and 2 V (solid line) for the Ti-MoS$_2$ contact geometry. The variable $\Phi_P$ refers to the bias-dependent potential barrier induced by the Ti contact. (c) Same as (b), but for the Ti-TiO$_2$-MoS$_2$ configuration. The TiO$_2$ layer measures 1 nm in all cases, a value large enough to capture the relevant physics, but thin enough to remain computationally affordable.

its rutile, well-ordered phase. To compensate for this idealization, the TiO$_2$ CB edge had to be manually raised to 0.15 eV above the MoS$_2$ one, which corresponds to the experimentally determined band offset. The adjusted band diagram is presented in Fig. 2 where it can also be seen that the non-altered Schottky barrier heights, with (0.29 eV) and without (0.17 eV) TiO$_2$, are close to the experimental ones (0.23 eV).

After scaling up the Ti-MoS$_2$ and Ti-TiO$_2$-MoS$_2$ unit cells, contact geometries similar to the one shown in Fig. 3(a) were built up and a 3nm thick HfO$_2$ layer was added to serve as back gate dielectric. The MLWF Hamiltonian matrices of these systems were inserted
into a dissipative NEGF quantum transport solver that returns the current as a function of the applied voltages for a given electrostatic potential. The Green’s Functions must be evaluated for all possible electron energy $E$ and momentum $k_z$ pairs before summing up these contributions to give rise to the electron density. To reduce the heavy computational burden associated with NEGF simulations expressed in a MLWF basis, the process was simplified by pre-computing the electrostatic potential with a properly calibrated quantum mechanical solver based on the effective mass picture and by including only one momentum point carrying a representative current density. These approximations, together with the TiO$_2$ band edge shift, might limit the accuracy of the computed data. Since we focus on a qualitative description of the contact physics, the conclusions of the paper are not affected. More details about the simulation approach can be found in the Supporting Information.

Vertical cuts of the electrostatic potential energy across the Ti-MoS$_2$ and Ti-TiO$_2$-MoS$_2$ heterojunctions are depicted in Figs. 3(b) and (c), respectively, at two different back gate voltages $V_{gs}=0$ and 2 V. Of particular interest is the response of the MoS$_2$ monolayer. Without TiO$_2$, a potential barrier $\Phi_P$ of about 0.5 to 0.6 eV forms at the Ti/MoS$_2$ interface, on top of the already existing Schottky barrier $\Phi_B=0.166$ eV (see Fig. 2). The origin of $\Phi_P$ can be traced back to the penetration of the Ti wavefunctions into the MoS$_2$ band gap, which induces an additional electron density of $\sim 3e14$ cm$^{-2}$ in MoS$_2$. In Ref. it was inferred that this phenomenon leads to a metallization of MoS$_2$ and that the created states can carry current, thus causing an area-dependent injection of electrons below the Ti contact. It should however be noted that the electrons within the MoS$_2$ band gap result from exponentially decaying wavefunctions, with a large imaginary component of their wavevector along all directions. As these carriers cannot propagate, they only marginally contribute to the total current. Hence, speaking of a metallization of the MoS$_2$ monolayer does not appear justified when the involved electrons are not mobile. The large excess electron density in MoS$_2$ has nevertheless two important consequences: (i) it pushes up the electrostatic potential energy by $\Phi_P$, which acts as a barrier and blocks the transfer of electrons from the Ti electrode
Figure 4: (a) Current flowing through the Ti-MoS$_2$ contacts in Fig. 3 at $V_{gs} = 2$ V and $V_{ds} = 2$ V as a function of the overlap length $L_{overlap}$. The inset shows that the current (green arrow) is transferred from Ti to MoS$_2$ at the contact edge. (b) Spatially resolved current along the $x$-axis in the Ti and MoS$_2$ regions of the structure with $L_{overlap} = 19.7$ nm. An abrupt transfer from Ti to MoS$_2$ can be observed at the contact edge. (c) Spectral current distribution corresponding to sub-plot (b). Red indicates high current concentrations, green zero current. The blue line refers to the MoS$_2$ conduction band edge, the dashed line to the Fermi level, and the dashed rectangle, the electron tunneling window. (d-f) Same as (a-c), but for the Ti-TiO$_2$-MoS$_2$ contacts. Since the current depends on the metal/MoS$_2$ overlap length, the whole process becomes area- and no more edge-dependent. This can be best seen by the gradual current transfer between Ti and MoS$_2$ in (e).

to the MoS$_2$ layer in the overlap region (high transfer resistance) and (ii) it partly pins the Fermi level of the 2-D channel by screening the influence of the back gate voltage.

The situation is radically different in the presence of an interfacial TiO$_2$ layer. The oxide prevents the penetration of the Ti wavefunctions into MoS$_2$ and even depletes the electron population in the overlap region, under flat band conditions. Due to this, the MoS$_2$ conduction band can be readily modulated by the back gate voltage and pushed below the metal Fermi level, thereby making itself accessible for electrons tunneling through the oxide. This lowers the transfer resistance from Ti to MoS$_2$. The usage of such Fermi level de-pinning layer has been recently demonstrated for Co/h-BN electrodes.\textsuperscript{44}
Using these electrostatic potentials, the current flowing through the assembled Ti-contacted MoS$_2$ structures was computed at a back gate voltage $V_{gs}=2$ V and a source-to-drain voltage $V_{ds}=2$ V measured between the Ti region on the left ("source") and the MoS$_2$ single-layer on the right ("drain"). Figure 4 unveils the behavior of the electrical current as a function of the (i) metal-semiconductor overlap length $L_{\text{overlap}}$, (ii) region where it flows (Ti or MoS$_2$), and (iii) energy at which it is carried. It clearly appears that when Ti and MoS$_2$ are in direct contact, the current becomes independent of $L_{\text{overlap}}$ and stays constant (Fig. 4(a)). There is almost no current exchange between the top electrode and the bottom 2-D material because of the blocking potential barrier discussed above, except at the edge of the Ti/MoS$_2$ interface (Fig. 4(b)) where the combined effect of $V_{gs}$ and $V_{ds}$ pushes down the MoS$_2$ conduction band. This opens up a tunneling window for the electrons situated in the Ti electrode, as can be seen in Fig. 4(c), activating a near-edge injection process whose efficiency hinges on the characteristic (or screening) length $\lambda_c$ of the contact. Here, due to the ultra-thin bottom HfO$_2$ layer, $\lambda_c$ does not exceed 5 nm, but in real devices, it is typically much longer.

The presence of an interfacial TiO$_2$ layer completely changes the transfer mechanism. The current through the junction linearly increases with the overlap length $L_{\text{overlap}}$ before slowly saturating, as reported in Fig. 4(d). By extrapolating this plot, a transfer length $L_T \sim 150$ nm can be estimated. Figure 4(e) reveals that the electrical current gradually enters the MoS$_2$ monolayer from the top metallic contact, over the entire overlap region, which is a clear signature of an area-dependent injection process: the longer the contact, the higher the current magnitude. Although the quantitative $I_d$ values should be taken with precaution because of the applied modeling approximations, in particular the consideration of one single $k_z$ point, the performance of both contact configurations can still be compared to each other. First, it can be observed in Fig. 4(c) that without TiO$_2$, the current distribution remains fairly homogeneous in the pure Ti and Ti-MoS$_2$ overlap regions before losing energy when entering the MoS$_2$-only extension due to phonon emission. When a TiO$_2$ layer is inserted, phonon-assisted tunneling dominates the Ti-to-MoS$_2$ electron transfer, as indicated by the
current distribution in Fig. 4(f). This trend is confirmed when looking at the ballistic current, which is 2.5 times lower than the one with electron-phonon scattering.

From Fig. 4, it is also apparent that the total injected current is larger without the TiO$_2$ oxide layer despite the high Ti-MoS$_2$ transfer resistance caused by the interface potential barrier in the overlap region. This can be explained on one hand by the fact that electrons following the diagonal path shown in the inset of Fig. 4(a) move through a typical Schottky contact whose triangular shape can be modulated by the applied gate-to-source voltage. In this case, a larger characteristic length $\lambda_c$, as encountered in real devices, would significantly decrease $I_d$ by making the tunneling distance from Ti to MoS$_2$ longer. On the other hand, when TiO$_2$ is present, electrons must tunnel through this oxide to reach the 2-D channel, which reduces the transfer probability. A thinner, more transparent, interfacial layer, e.g. h-BN, could enhance the current magnitude.

It remains to put our work into perspective with literature. As already mentioned above, the metallization of MoS$_2$ below Ti contacts proposed in Ref. 23 does not support an area-dependence of the electron injection. On the contrary, it pins the Fermi level and deteriorates the modulation of the electrostatic potential in the overlap region. The experimental data of Refs. 32 and 33 agree with our results if we assume that there is a TiO$_2$ oxide layer between Ti and MoS$_2$ in the former case, whereas the interface is devoid of any oxide layer in the latter due to the higher vacuum deposition conditions. The modeling-based Ref. 34 postulated a near-edge injection process because a pure Ti-MoS$_2$ stack (without TiO$_2$) was simulated. The same was found in Ref. 35 for top contacts on a single-layer of MoS$_2$. However, the authors of this paper noticed a transition from an edge- to an area-dependent process as the MoS$_2$ thickness was increased, implying that any interfacial layer could be beneficial as long as it attenuates the penetration of the metal wavefunction into the band gap of the bottom semiconductor layer(s).

In conclusion, we have used ab initio simulations to demonstrate that the injection of electrons from a top metallic contact into an underlying 2-D material can occur either at
the edge or through the metal-semiconductor overlap area, depending on the presence or not of an interfacial layer. In this paper, Ti electrodes deposited on a MoS$_2$ layer, with and without an intermediate TiO$_2$ oxide, have served as an example to illustrate the physics at play. This finding can in principle be generalized to any blocking layer placed at the interface between a top contact and a 2-D monolayer, intentionally or not. Such a layer can hinder the penetration of the wavefunction originating from the metal into the band gap of the semiconductor, thus enabling an area-dependent transfer process. It can be envisioned that by engineering the properties of the interfacial layer the contact resistance of FETs based on 2-D semiconductors could be reduced, for example by selecting a material with a conduction band edge well-aligned with that of the 2-D crystal. Mobile electrons could then be directly injected into the transistor channel, without tunneling. At the same time, the charges pinning the Fermi level would still be stopped by the interfacial layer.

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**Supporting Information Available**

The following files are available free of charge. Detailed description of the modeling approach and of the applied approximations.
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