Research Article

Frequency Aliasing-Based Spatial-Wavenumber Filter for Online Damage Monitoring

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1. Introduction

According to the concept of smart material structure, structural health monitoring (SHM) technology involves the application of embedded sensor networks to obtain information related to structural health online. The characteristic parameters of the signal related to structural health are extracted by an advanced signal processing algorithm. Thus, we can determine whether the structure is damaged, localize the damage, analyze the degree of damage, and predict the failure form and remaining life of the damaged structure. Therefore, SHM technology can be used to prevent the occurrence of major accidents, improve safety of the structure, and reduce economic losses [1, 2]. As a type of elastic stress wave, the Lamb wave is widely applied in damage identification of composite structures because of its long propagation distance, small energy attenuation, and sensitive response to damage. Therefore, SHM technology based on the Lamb wave has been widely studied and is one of the most promising SHM technologies. In such applications, the Lamb wave is excited and collected by a low-cost piezoelectric transducer (PZT) sensor [3–5].

In the existing SHM technologies, the damage imaging method which has high signal-to-noise ratio can visually indicate damage location and size. Examples of these imaging techniques include the delay-and-sum method [6–9], time reversal method [10–13], probabilistic diagnostic algorithm [14–17], phased array method [18–21], multisignal classification method [22–26], and spatial-wavenumber filter method [27–35]. Among them, the spatial-wavenumber filter method, which has been extensively studied, can extract the specific mode of the Lamb wave, distinguish the incident wave and damage scattering wave, and reduce the overlap of Lamb wave signals [33–35]. Purekar and Pines [27] introduced the spatial-wavenumber filter into the Lamb wave and linear PZT sensor array based damage imaging first.
and performed damage monitoring of large aluminum plates based on the wavenumber of the Lamb wave signal acquired by structural mechanical modeling. Wang et al. [28] improved the spatial-wavenumber filter independent of the structural material parameters using the envelope of Lamb wave damage scattering signal extracted by the Hilbert transform. Qiu et al. [29, 30] studied a scanning spatial-wavenumber filter for damage and impact localization of composite structures without using the structural model. Ren et al. [31, 32] extended the model-independent spatial-wavenumber filter to multidamage and impact monitoring using eigenvalue decomposition and wavenumber searching.

In previous spatial-wavenumber filter damage imaging research, the Lamb wave was collected using linear PZT sensor array. According to the Nyquist–Shannon sampling theorem, the frequency of the Lamb wave must be less than half of the sampling frequency. Similarly, the wavenumber of the Lamb wave also must be less than half of the spatial sampling wavenumber. However, the diameter of PZT sensor which is difficult to increase limits the spatial sampling wavenumber. Thus, it will limit the application of spatial-wavenumber filter based online damage monitoring. In this study, a frequency aliasing based spatial-wavenumber filter for online damage monitoring is proposed, which extends the spatial-wavenumber filtering range to the spatial sampling wavenumber. The basic principle of the spatial-wavenumber filter is introduced in Section 2. Then, the damage is localized using the spatial-wavenumber filter and cruciform PZT sensor array that is described in Section 3. The proposed spatial-wavenumber filter is validated on an epoxy laminate plate in Section 4. Finally, the conclusions are stated in Section 5.

2. Spatial–Wavenumber Filter

2.1. Theoretic Foundation. Figure 1 shows a linear PZT sensor array placed on a structure. There are $M$ PZTs in the linear PZT sensor array and are numbered $m = 1, \ldots, M$. The spatial sampling interval is $\Delta x$, which is also equivalent to the distance between the centers of two adjacent PZT sensors in the linear PZT sensor array. A Cartesian coordinate was built on the structure. The original point was set at the center point of the linear PZT sensor array, and the $X$-axis was set along the linear PZT sensor array.

As illustrated in Figure 1, the acoustic source located at $(\theta_a, L_a)$ excites the Lamb wave signal in the structure. The acoustic source is in the far-field area of the linear PZT sensor array. The propagation of the Lamb wave in the structure can be expressed using [36]

$$ f(x, t) = A \cdot e^{i(\omega_a t - k_x x + \phi_0)}, \tag{1} $$

where $x$ and $t$ represent the propagation distance and time of the Lamb wave, respectively; $A$ denotes the amplitude term of the Lamb wave; $\omega_a$ and $k_x$ are the central frequency and wavenumber of the Lamb wave; $\phi_0$ is the initial phase of the Lamb wave.

The wavenumber response can be obtained by Fourier Transform of the spatial response shown in (1) and (2). Then, the wavenumber domain of the Lamb wave can be obtained as follows:

$$ F(k) = \int_{-\infty}^{\infty} f(x, t) \cdot e^{-ikx} \, dx, $$

$$ = \int_{-\infty}^{\infty} B \cdot e^{ik_0 x} \cdot e^{-ikx} \, dx, \tag{2} $$

$$ = B \cdot 2\pi \cdot \delta(k - k_0), $$

where $\delta$ is the Dirac function and

$$ B = A \cdot e^{i(\omega_a + \phi_0)}. \tag{3} $$

Using the linear PZT sensor array, the discrete spatial sampling signal $f'(x, t)$ can be obtained by spatial sampling of Lamb wave with a spatial sampling interval of $\Delta x$, as shown in (4). In other words, the spatial sampling signal $f'(x, t)$ is the product of the Lamb wave propagating continuously and the periodic impact signal $p(x)$:

$$ f'(x, t) = f(x, t) \cdot p(x), $$

$$ = B \cdot e^{ik_0 x} \cdot \sum_{n=-\infty}^{\infty} \delta(x - n \cdot \Delta x), \tag{4} $$

$$ = B \cdot \sum_{n=-\infty}^{\infty} e^{ik_0 n \Delta x} \cdot \delta(x - n \cdot \Delta x), $$

where $n$ is an integer and

$$ p(x) = \sum_{n=-\infty}^{\infty} \delta(x - n \cdot \Delta x). \tag{5} $$

Using the Fourier Transform, the wavenumber response $P(x)$ of the periodic impact signal $p(x)$ can be obtained, as shown in

$$ P(k) = \int_{-\infty}^{\infty} P(x) \cdot e^{-ikx} \, dx, $$

$$ = \frac{2\pi}{\Delta x} \sum_{n=-\infty}^{\infty} \delta(k - n \cdot k_x), \tag{6} $$

where $k_x = 2\pi/\Delta x$ is the spatial sampling wavenumber of the linear PZT sensor array.
According to (2) and (6), the wavenumber response of the discrete spatial sampling signal \( f(x, t) \) is shown in
\[
F'(k, t) = \int_{-\infty}^{\infty} f(x, t) \cdot p(x) \cdot e^{-i k x} \, dx,
\]
\[
= \frac{1}{2\pi} \cdot S(k) \otimes P(k),
\]
where \( \otimes \) is the convolution operator. Equation (7) shows that in the range of wavenumber domain \((-k_a, k_a)\) we have the following:

1. **\( k_a \geq 0 \):**
   - (a) If \( k_a \geq 2k_n \), the wavenumber results of the discrete spatial sampling signal \( f(x, t) \) are \( k_a \) and \((k_a - k)\), and \((k_a - k) \in (-k_a, k_a)\), which is negative.
   - (b) If \( k_a \leq k_c < 2k_n \), the wavenumber results of the discrete spatial sampling signal \( f(x, t) \) are \( k_a \) and \((k_a - k)\), and \((k_a - k) \in (-k_a, 0)\), which is negative.
   - (c) If \( 0.5k_a < k_c < k_a \), the wavenumber results of the discrete spatial sampling signal \( f(x, t) \) are \( k_a \) and \((k_a - k)\), and \((k_a - k) \in (0, k_a)\), which is positive, and \((k_a - 2k)\) \( \in (-k_a, 0)\), which is negative.

2. **\( k_a < 0 \):**
   - (a) If \( k_a \geq 2k_n \), the wavenumber results of the discrete spatial sampling signal \( f(x, t) \) are \( k_a \) and \((k_a + k)\), and \((k_a + k) \in (k_a, k_a)\), which is negative.
   - (b) If \( |k_a| < k_n \), the wavenumber results of the discrete spatial sampling signal \( f(x, t) \) are \( k_a \) and \((k_a + k)\), and \((k_a + k) \in (0, k_a)\), which is positive.
   - (c) If \( 0.5k_a < k < |k_a| \), the wavenumber results of the discrete spatial sampling signal \( f(x, t) \) are \( k_a \) and \((k_a + 2k)\), and \((k_a + 2k) \in (0, k_a)\), which is positive, and \((k_a + 4k)\) \( \in (-k_a, 0)\), which is negative.

As discussed above, the spatial sampling wavenumber \( k_n \) should be greater than twice that of the Lamb wave according to the Nyquist–Shannon sampling theorem, as shown in (8). Furthermore, there is only one calculated wavenumber result \( k_n \) in the range of \((-0.5k_a, 0.5k_a)\) which is the wavenumber \( k_n \) of the Lamb wave in the previous research:
\[
k_c > 2k_n, \quad (8)
\]

Therefore, if \( k_c \neq 0 \), there will be two calculated wavenumber results \( k_n \) and \((k_n - k)\) \((k_n + k)\) in the range of \((-k_a, k_a)\) and \( k_c > 2k_n \) or \( |k_n| \leq k_c < 2k_n \). The signs of the two calculated wavenumber results are opposite. Thus, the wavenumber \( k_n \) of the Lamb wave can be obtained when the sign of the wavenumber \( k_n \) can be determined.

2.2. Principle of the Method. As shown in Figure 1, the spatial sampling wavenumber of the linear PZT sensor array exceeds that of the Lamb wave, \( k_c > |k_n| \). In addition, the received Lamb wave signals collected by the linear PZT sensor array can be expressed as shown in
\[
f'(x_m, t) = B \cdot e^{-i k_n x_m} \cdot e^{i k_n \cos \theta_n x_m} = C \cdot e^{i k_n \cos \theta_n x_m} \quad (m = 1, \ldots, M),
\]
where \( \vec{L}_a \) is the vector of the distance \( L_a \) from the position of the acoustic source to the origin point; \( \vec{X}_m \) is the vector of the X-axis coordinate \( x_m \) of the No. \( m \) PZT sensor:
\[
C = B \cdot e^{-i k_n L_a}. \quad (10)
\]

According to (7), the received Lamb wave signal shown in (9) is transformed to the wavenumber response, as shown in
\[
F''(k, t) = \frac{C \cdot 2\pi}{\Delta x} \sum_{n=-\infty}^{\infty} \delta(k - k_a \cdot \cos \theta - n \cdot k_c) \quad (11)
\]

A spatial-wavenumber filter is designed for the received Lamb wave signal, as shown in (12). Using Fourier Transform, the wavenumber response of the spatial-wavenumber filter can be obtained, as shown in
\[
\Phi_{k'}(x) = e^{i k' x}, \quad (12)
\]
\[
\Phi(k) = \int_{-\infty}^{\infty} \Phi_{k'}(x) \cdot e^{-i k x} \, dx, \quad (13)
\]
\[
= 2\pi \cdot \delta(k - k'), \quad (13)
\]
where \( k' \) is the pass-through wavenumber of the spatial-wavenumber filter.

Equation (13) shows that the spatial-wavenumber filter can selectively pass through the signal with the wavenumber that is \( k = k' \) and reject the signal with the other wavenumbers \( k \neq k' \).

Next, the designed spatial-wavenumber filter is applied to the received Lamb wave signal when the wavenumber filtering range is \((-k_a, k_a)\), as shown in (14). The filtered wavenumber response of the received Lamb wave signal can be expressed as
\[
h_{k'}(x_m, t) = f'(x_m, t) \otimes \Phi_{k'}(x_m) \quad (14)
\]
\[
H(k, t) = 2\pi \cdot \delta(k - k') \quad (15)
\]
\[
= \frac{C \cdot 2\pi}{\Delta x} \sum_{n=-\infty}^{\infty} \delta(k - k_a \cdot \cos \theta - n \cdot k_c) \quad (15)
\]

Finally, the spatial-wavenumber filtered synthesis signal of the linear PZT sensor array can be obtained using
\[
h'(k', t) = \sum_{m=1}^{M} |f'(x_m, t) \otimes \Phi_{k'}(x_m)|. \quad (16)
According to (15), the amplitude value of the spatial-wavenumber filtered synthesis signal is small when $k' \neq (k_c \cos \theta_a - n \cdot k_s)$. When $k' = (k_c \cos \theta_a - n \cdot k_s)$, the amplitude value will be maximum. Therefore, by applying the designed spatial-wavenumber filter to the Lamb wave received signal with the wavenumber filtering range from $-k_s$ to $+k_s$, the $(k_c \cos \theta_a - n \cdot k_s)$ value corresponding to the maximum value of spatial-wavenumber filtered synthesis signal can be obtained.

According to the analysis in the previous section, there are two positive and negative wavenumber results in the range of $(-k_c, k_c)$ when $k_c \cos \theta_a > 0$. If $k_c \cos \theta_a < 0$, $(k_c \cos \theta_a + k_s)$ will be negative. If $k_c \cos \theta_a < 0$, $(k_c \cos \theta_a - k_s)$ will be negative.

There will be only one value of $0 \text{rad/m}$ which can be obtained when $k_c \cos \theta_a = 0$, which is the wavenumber of the received Lamb wave signal collected by the linear PZT sensor array.

In addition, Figure 1 shows that if the damage is at the right side of the Y-axis, that is, the positive half axis of the X-axis, the arrival time of the received Lamb wave signal collected by the No.$M$ PZT sensor will be earlier than that of the signal collected by the No.1 PZT sensor and $k_c \cos \theta_a > 0$. Otherwise, the arrival time of the Lamb wave received signal collected by the No.$M$ PZT sensor will be later than that of signal collected by the No.1 PZT sensor and $k_c \cos \theta_a < 0$, when the damage is at the left side of the Y-axis. Therefore, when the spatial-wavenumber filtering result has two values, the wavenumber of the received Lamb wave signal can be finally determined by comparing the arrival times of the received Lamb wave signals collected by the No.$M$ and No.1 PZT sensors in the linear PZT sensor array.

In practical application, the spatial-wavenumber filtering result and the calculated arrival time considerably fluctuate because of various factors which can easily cause misjudgment. Therefore, the average arrival time difference $t_a$ between two adjacent sensors can be calculated using

$$t_a = \frac{\sum_{m=1}^{M-1} (t_{m+1} - t_m)}{M - 1}$$

(17)

where $t_m$ is the arrival time of the received Lamb wave signal collected by the No.$m$ PZT sensor and $t_{m+1}$ is the arrival time of the received Lamb wave signal collected by the No.$(m+1)$ PZT sensor.

Equation (17) shows that the arrival time of the received Lamb wave signals collected by the No.$M$ PZT sensor will be later than that of the signal collected by the No.1 PZT sensor if $t_a > 0$, which means $k_c \cos \theta_a < 0$. Otherwise, if $t_a < 0$, the arrival time of the received Lamb wave signals collected by the No.$M$ PZT sensor will be earlier than that of signal collected by the No.1 PZT sensor and $k_c \cos \theta_a > 0$.

Finally, the wavenumber of the received Lamb wave signal can be obtained.

Using the linear PZT sensor array, the received Lamb wave signals can be collected for a certain length of time. Then, a wavenumber-time image can be obtained by spatial-wavenumber filtering of the received Lamb wave signals at each time, as shown in Figure 2. In Figure 2, the wavenumber and time corresponding to the image point of the highest pixel value can be judged to be the spatial-wavenumber filtering result $(k_c \cos \theta_a - n \cdot k_s)$ and the arrival time $t_R$ of the received Lamb wave signal. Therefore, the wavenumber $k_c \cos \theta_a$ and the arrival time $t_R$ of the Lamb wave received signal can be obtained simultaneously by the spatial-wavenumber filter.

3. Damage Localization

There is a cruciform PZT sensor array in the structure which is constructed by two linear PZT sensor arrays, as shown in Figure 3. The two linear PZT sensor arrays of the cruciform PZT sensor array are labeled as No.1 and No. II. A Cartesian coordinate is built on the structure. The original point is set at the cross point of the cruciform PZT sensor array, and the X- and Y-axis are set along the No.1 and No. II PZT sensor arrays. The Lamb wave is excited from the center point and propagation in the structure. If there is damage in the structure, it will scatter the incident Lamb wave [37]. The damage scattering signal can be collected by the cruciform PZT sensor array for a certain length of time.

The values of $k_{a-1} = k_c \cos \theta_a$ and $t_{R-1}$ can be obtained by spatial-wavenumber filtering of the damage scattering signal collected by No.1 linear PZT sensor array, as shown in Figure 3. In addition, $k_{a-II} = k_c \cos (90° - \theta_a)$ and $t_{R-II}$ can be obtained by spatial-wavenumber filtering of the damage scattering signal collected by No. II linear PZT sensor array. Thus, the X-axis and Y-axis projection wavenumbers of the damage scattering signals all can be calculated using the spatial-wavenumber filter and cruciform PZT sensor array. Then, the angle $\theta_a$ of damage can be calculated using (18).

Furthermore, the distance $L_a$ of damage can be calculated using the following equation. Finally, the damage position $(\theta_a, L_a)$ is localized:

$$L_a = \frac{1}{2} \cdot c_g \cdot \left( t_{R-II} + t_{R-1} - t_e \right)$$

(19)

where $c_g$ is the Lamb wave group velocity and $t_e$ is the Lamb wave start time.
4. Validation of the Method

4.1. Experimental Setup. The validation experimental system comprises an integrated SHM system, a cruciform PZT sensor array, and an epoxy laminate plate, as shown in Figure 4.

The dimensions of the epoxy laminate plate are 60 cm × 60 cm × 0.2 cm (length × width × thickness). The ply sequences are [0/90/0/90/0/90]. The cruciform PZT sensor array is arranged in the middle of the lower part of the epoxy laminate plate. The two linear PZT sensor arrays of the cruciform PZT sensor array are numbered No.I and No.II. Each linear PZT sensor array consists of 7 PZT-5A sensors. The spatial sampling interval which is also the distance between the center points of two adjacent PZT sensors is Δx = 0.9 cm. The PZT sensors in No.I PZT sensor array are labeled as PZT I-1, . . . , PZT I-7. The PZT sensors in No.II PZT sensor array are labeled as PZT II-1, . . . , PZT II-7. A PZT sensor is pasted on the back of the specimen and the cross point of the cruciform PZT sensor array as the excitation element of the Lamb wave. The cross point of the cruciform PZT sensor array is 20 cm from the lower boundary of the epoxy laminate plate and 30 cm from the left and right boundaries of the epoxy laminate plate. The original point is set at the cross point of the cruciform PZT sensor array. In addition, the X- and Y-axis of the Cartesian coordinates are set along the No.I PZT sensor array and No.II PZT sensor array, respectively. The Lamb wave velocity $c_g$ is measured by a PZT sensor pasted at the position of 90° and 30 cm, which is labeled as PZT 8. The integrated SHM system is developed by Professor Yuan research group [38].

In this experimental verification, the excitation signal was a modulated 5-peak narrowband signal [39]. The frequency and amplitude of the excitation signal are 50 kHz and $\pm 70$ V. The sampling frequency and length of the Lamb wave are 10 MHz and 8000 samples with 1000 presamples.

The experimental process is as follows: first, the Lamb wave velocity $c_g$ is measured using the Shannon wavelet transform [40]. The Lamb wave is excited by the excitation PZT sensor and propagates in the epoxy laminate plate. The Lamb wave signals collected by the cruciform PZT sensor array are shown in Figure 6.

After the damage $F$ is applied to the epoxy laminate plate, the online monitoring signals $f_{OM}$ collected by the cruciform PZT sensor array are shown in Figure 6.

4.2. Damage Localization. The damage $F$ is chosen as an example to validate in detail the proposed method and is located at 180° and 20 cm. First, the health reference signals $f_{HR}$ are collected by the cruciform PZT sensor array, as shown in Figure 5.

After the damage $F$ is applied to the epoxy laminate plate, the online monitoring signals $f_{OM}$ collected by the cruciform PZT sensor array are shown in Figure 6.
The damage scattering signals of damage $F$ can be extracted by subtracting the health reference signals $f_{HR}$ from the online monitoring signals $f_{OM}$, as shown in Figure 7.

According to the spatial sampling interval $\Delta x = 0.9$ cm, the wavenumber filtering range was set to be from $-680$ rad/m to $680$ rad/m with the wavenumber filtering interval $\Delta k = 0.1$ rad/m. Then, the wavenumber-time images of
damage $F$ can be obtained by spatial-wavenumber filtering of
the damage scattering signals extracted from the online
monitoring signals, as shown in Figure 8.

In Figure 8(a), two wavenumber filtering results
($-387.9$ rad/m and $310.3$ rad/m) are shown that correspond
to the point of the maximum value. Because there are two
wavenumber filtering results of No.I PZT sensor array, the
average arrival time difference ($t_a = 0.0025$ ms) between two
adjacent sensors of No.I PZT sensor array can be calculated.
Then, $k_{a,1} = -387.9$ rad/m is selected as the wavenumber of
damage scattering signals collected by No.I PZT sensor array for
$t_a = 0.0025 > 0$. Furthermore, the arrival time of the
damage scattering signals collected by No.I PZT sensor array
is $t_{R,1} = 0.4029$ ms.

The wavenumber ($k_{a,II} = 3.9$ rad/m) and arrival time
($t_{R,II} = 0.3992$ ms) of the damage scattering signals collected
by No.II PZT sensor array can also be obtained from
Figure 8(b).

According to (18), the damage direction ($\theta_a = 179.4^\circ$) can
be obtained using the wavenumbers $k_{a,1}$ and $k_{a,II}$, and the
damage direction error is $-0.6^\circ$.

The excitation time ($t_e = 0.1031$ ms) of the Lamb wave is
calculated by the continuous complex Shannon wavelet
transform. Then, the distance $L_a = 20.4$ cm of the damage $F$
can be calculated by (19). Finally, the damage position
($179.4^\circ$ and $20.4$ cm) is localized, and the damage localization
error becomes $\Delta l = 0.5$ cm.

According to the signal processing flow of damage $F$
discussed above, the six damage localization results and
errors are listed in Table 1, and the damage localization
image is shown in Figure 9. It can be seen from Table 1 that
the X-axis projection wavenumbers of damages $A$ and $F$
Figure 8: Wavenumber-time images of damage F. (a) No.1 PZT sensor array. (b) No.2 PZT sensor array.

The epoxy laminate plate

Figure 9: The damage localization image of the six damages.

Figure 10: Wavenumber-time images of the conventional spatial-wavenumber filter method. (a) $k_{a-1}$ of damage A; (b) $k_{a-1}$ of damage F.
exceed half of the spatial sampling wavenumber; the wavenumber-time images obtained by the conventional spatial-wavenumber filter method [29, 30], with the wavenumber filtering range from \(-340 \text{ rad/m}\) to \(340 \text{ rad/m}\), are shown in Figure 10. In Figure 10, the X-axis projection wavenumber of damage \(A\) is \(k_{a1} = -315.8 \text{ rad/m}\), and the damage direction is \(\theta_A = 169.5°\) with the damage direction error 159.5°. Similarly, the X-axis projection wavenumber of damage \(F\) is \(k_{f1} = 310.3 \text{ rad/m}\), and the damage direction is \(\theta_F = 0.7°\) with the damage direction error 179.3°. It means that if the wavenumber of collected signal exceeds half of the spatial sampling wavenumber, the damage direction cannot be acquired correctly.

In the proposed method, the maximum filtering wavenumber is set to the spatial sampling wavenumber, and the two wavenumber filtering results are distinguished according to the average arrival time difference. The maximum damage localization errors are less than 2 cm in this experiment. The results indicate that the proposed method can improve the limitation of Nyquist–Shannon sampling theorem to the conventional spatial-wavenumber filter method, expand the filtering range of spatial-wavenumber filter to the spatial sampling wavenumber of the linear PZT sensor array, and thus expand the application of the spatial-wavenumber filter based online damage monitoring.

5. Conclusion

In this paper, a frequency aliasing based spatial-wavenumber filter for online damage monitoring is proposed. In this method, the wavenumber filtering range of the spatial-wavenumber filter is expanded to the spatial sampling wavenumber of the Lamb wave. Then, the wavenumber of the received Lamb wave signal is determined according to the average arrival time difference between two adjacent sensors in a linear PZT sensor array. The damage can be localized using this method and a cruciform PZT sensor array. We validated the results using an epoxy laminate plate, and the results show that the damage localization errors are less than 2 cm. This method extends the wavenumber processing ability of the linear PZT sensor array using a software algorithm, without adding any hardware equipment. It is easily expanding the application of the spatial-wavenumber filter based online damage monitoring. However, depending on the group velocity of damage localization, the application of the proposed method may be limited; hence, further study is required. In addition, the influence of various factors on this method also needs to be studied further.

Data Availability

The data used to support the findings of this study are available from the corresponding author upon request.

Conflicts of Interest

The authors declare no conflicts of interest.

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