A KINEMATIC STUDY OF THE ANDROMEDA DWARF SPHEROIDAL SYSTEM

MICHELLE L. M. COLLINS\textsuperscript{1,2}, SCOTT C. CHAPMAN\textsuperscript{2,3}, R. MICHAEL RICH\textsuperscript{4}, RODRIGO A. IBATA\textsuperscript{5}, NICOLAS F. MARTIN\textsuperscript{1,5}, MICHAEL J. IRWIN\textsuperscript{2}, NICHOLAS F. BATE\textsuperscript{6}, GERARD F. LEWIS\textsuperscript{6}, JORGE PEÑARRUBIA\textsuperscript{7,8,15}, NOBUO ARIMOTO\textsuperscript{9,10}, CAITLIN M. CASEY\textsuperscript{11}, ANNETTE M. N. FERGUSON\textsuperscript{8}, ANDREAS KOC\textsuperscript{12}, ALAN W. MCCONNACHIE\textsuperscript{13}, AND NIAL TANVIR\textsuperscript{14}

\textsuperscript{1} Max-Planck-Institut für Astronomie, Königstuhl 17, D-69117 Heidelberg, Germany
\textsuperscript{2} Institute of Astronomy, Madingley Rise, Cambridge CB3 0HA, UK
\textsuperscript{3} Dalhousie University Department of Physics and Atmospheric Science Coburg Road, Halifax B3H1A6, Canada
\textsuperscript{4} Department of Physics and Astronomy, University of California, Los Angeles, CA 90095-1547, USA
\textsuperscript{5} Observatoire astronomique de Strasbourg, Université de Strasbourg, CNRS, UMR 7550, 11 rue de l'Université, F-67000 Strasbourg, France
\textsuperscript{6} Sydney Institute for Astronomy, School of Physics, A28, University of Sydney, NSW 2006, Australia
\textsuperscript{7} Instituto de Astrofísica de Andalucía-CSIC, Glorieta de la Astronomía s/n, E-18008 Granada, Spain
\textsuperscript{8} Institute for Astronomy, University of Edinburgh, Royal Observatory, Blackford Hill, Edinburgh EH9 3HJ, UK
\textsuperscript{9} Subaru Telescope, National Astronomical Observatory of Japan, 650 North A'ohoku Place, Hilo, HI 96720, USA
\textsuperscript{10} Graduate University for Advanced Studies, 2-21-1 Osawa, Mitaka, Tokyo 181-8588, Japan
\textsuperscript{11} Institute for Astronomy, 2680 Woodlawn Drive, Honolulu, HI 96822-1839, USA
\textsuperscript{12} Zentrum für Astronomie der Universität Heidelberg, Landessternwarte, Königstuhl 12, D-69117 Heidelberg, Germany
\textsuperscript{13} NRC Herzberg Institute of Astrophysics, 5071 West Saanich Road, British Columbia, Victoria V9E 2E7, Canada
\textsuperscript{14} Department of Physics & Astronomy, University of Leicester, University Road, Leicester LE1 7RH, UK

Received 2012 November 16; accepted 2013 February 25; published 2013 April 26

ABSTRACT

We present a homogeneous kinematic analysis of red giant branch stars within 18 of the 28 Andromeda dwarf spheroidal (dSph) galaxies, obtained using the Keck I/LRIS and Keck II/DEIMOS spectrographs. Based on their $g - i$ colors (taken with the CFHT/MegaCam imager), physical positions on the sky, and radial velocities, we assign probabilities of dSph membership to each observed star. Using this information, the velocity dispersions, central masses, and central densities of the dark matter halos are calculated for these objects, and compared with the properties of the Milky Way dSph population. We also measure the average metallicity ([Fe/H]) from the co-added spectra of member stars for each M31 dSph and find that they are consistent with the trend of decreasing [Fe/H] with luminosity observed in the Milky Way population. We find that three of our studied M31 dSphs appear as outliers in terms of their central velocity dispersion, And XIX, XXI, and XXV, all of which have large half-light radii ($\gtrsim700$ pc) and low velocity dispersions ($\sigma_v < 5$ km s$^{-1}$). In addition, And XXV has a mass-to-light ratio within its half-light radius of just $[M/L]_{\text{half}} \approx 10.3^{+7.0}_{-6.7}$, making it consistent with a simple stellar system with no appreciable dark matter component within its 1$\sigma$ uncertainties. We suggest that the structure of the dark matter halos of these outliers have been significantly altered by tides.

Key words: dark matter – galaxies: dwarf – galaxies: fundamental parameters – galaxies: kinematics and dynamics – Local Group

Online-only material: color figures, machine-readable table

1. INTRODUCTION

The underlying nature of the dark matter halos of dwarf spheroidal galaxies (dSphs) has garnered significant attention from the scientific community over the past decade. The goal of recent observational studies of these objects has been to make critical tests of structure formation scenarios, particularly focusing on the viability of the canonical ΛCDM model. There is the long standing issue of the relative dearth of these faintest of galaxies observed surrounding nearby galaxies when compared with the number of dark matter subhalos produced in $N$-body simulations, which is referred to as the “missing satellite” problem (Klypin et al. 1999; Moore et al. 1999). The extent to which this mismatch is considered problematic has decreased over recent years as both theorists and observers have sought to reconcile the simulated and observable universe. From a modeling point of view, one does not expect stars to be able to form within all dark matter subhalos seen in simulations, and at a certain mass limit ($V_{\text{max}} \lesssim 15$ km s$^{-1}$), see Peñarrubia et al. 2008a; Koposov et al. 2009), star formation is unable to proceed. Thus, there is a lower limit placed on galaxy formation. This mass limit is also tied to feedback processes that can remove the baryonic reservoirs required for star formation (e.g., Bullock et al. 2000, 2010; Somerville 2002; Kravtsov 2010; Nickerson et al. 2011; Kazantzidis et al. 2011). This would imply that only the most massive subhalos seen in simulations are able to form and retain luminous populations. Observers have also attempted to quantify current survey completeness and radial selection effects to account for the number of satellites we are not currently able to detect (e.g., Koposov et al. 2008; Tollner et al. 2008; Walsh et al. 2009). These studies suggest that there are of the order of a few hundred satellites within the Milky Way’s (MW) virial radius that we have yet to detect.

The high dark matter dominance of dSph galaxies also singles them out as objects of interest. With total dynamic mass-to-light ratios of $[M/L] \sim 10$–1000 s and half-light radii of $r_{\text{half}} \sim 10$–1000 pc, they are ideal systems with which to probe the inner density profiles of dark matter halos. Recent imaging and spectroscopic observations of these objects within the Local Group have shown that, despite spanning approximately
The Astrophysical Journal, 768:172 (36pp), 2013 May 10

Collins et al.

five decades in luminosity, the dSphs of the MW share a common mass scale and a universal density profile (Strigari et al. 2008; Walker et al. 2009b; Wolf et al. 2010). With a kinematic resolution of a few tens of parsecs, these objects allow us to start addressing the question of whether the central regions of these halos follow cuspy density profiles as predicted by cosmological simulations (Navarro et al. 1997), or constant density cores, similar to what is observed in low surface brightness galaxies (Blais-Ouellette et al. 2001; de Blok & Bosma 2002; de Blok et al. 2003; de Blok 2005; Swaters et al. 2003; Kassin et al. 2006; Spano et al. 2008). From studies of brighter dSphs, such as Sculptor and Fornax (Walker & Peñarrubia 2011; Amorisco & Evans 2012; Jardel & Gebhardt 2012) it appears that their halo density profiles are also inconsistent with hosting central cusps. It is possible that these objects originally formed with cuspy density profiles, and that these have been subsequently modified by baryonic feedback. If this is truly the case, one should be able to observe cuspy profiles in the fainter dSph population (Zolotov et al. 2012) as these do not contain enough baryons to drive this change in the dark matter density profile. Perhaps the only way to gain further insight into this contentious issue is by measuring the kinematics for large numbers of stellar tracers within these objects and analyzing them with detailed models that do not make ab initio assumptions about the underlying density profiles, or the velocity anisotropy of both the dark matter and stars, such as those employed by Walker & Peñarrubia (2011) and Jardel & Gebhardt (2012).

To date, the majority of studies involving the detailed kinematics of dSphs have revolved largely around those belonging to the MW, as these are nearby enough that we can measure the velocities of their member stars to a high degree of accuracy. However, there are currently only ∼25 known MW dSphs, with luminosities ranging from 10^2–10^7 L_☉. For the very faintest, some controversy remains as to whether they are massively dark-matter dominated (see, e.g., Niederste-Ostholt et al. 2009; Simon et al. 2011), but almost all of them have been shown to be consistent with the universal mass profiles of Walker et al. (2009a) and Wolf et al. (2010). One notable exception to this is the Hercules object (Adén et al. 2009), which some have argued is currently undergoing significant tidal disruption (Martin & Jin 2010). Andromeda represents the only other system for which comparable kinematic analyses can be performed. M31 now has 28 dSph companions known, whose luminosities range from ∼10^5–10^9 L_☉, the majority of which have been discovered by the Canada–France–Hawaii Telescope (CFHT) Pan-Andromeda Archaeological Survey (PAndAS; Martin et al. 2006, 2009; Ibata et al. 2007; Irwin et al. 2008; McConnachie et al. 2008; Richardson et al. 2011). The relatively brighter lower bound for the luminosities of M31 dSphs compared to the MW is a detection limit issue, rather than a sign of differing stellar populations (N. F. Martin et al. 2013, in preparation). It has been noted by a number of authors (e.g., McConnachie & Irwin 2006b; Tollerud et al. 2012; McConnachie 2012) that for the brighter dSphs (M_V < −8), those belonging to M31 are two to three times more extended in terms of their half-light (r_{half}) and tidal (r_t) radii compared with the MW. In these papers, the underlying cause of this discrepancy was not identified, but it has been argued that it could be an effect of environment, with the mass distribution of the host playing an important role. Subsequent work by Brassard et al. (2011a), who included the fainter, non-classic M31 dSphs for the first time, showed that statistically, the relationship between size and luminosity for dSphs in the MW and Andromeda are actually largely consistent with one another, however there remain a number of significantly extended outliers within the Andromedean system (e.g., And II, And IX, r_{half} ∼ 1.2 kpc and 1.5 kpc, respectively), and the scatter in this relationship is large (up to an order of magnitude at a given luminosity; McConnachie 2012). Working from the McConnachie & Irwin (2006b) results, Peñarrubia et al. (2008a) modeled the expected velocity dispersions for the M31 dSphs, assuming that all dSph galaxies are embedded within similar mass dark matter halos. A robust prediction of their modeling was that, given the larger radial extents, the dSphs of M31 should be kinematically hotter than their MW counterparts by a factor of ∼2. At the time of writing, they had only two measured velocity dispersions for the M31 dSphs, those of And II and And IX (Côté et al. 1999; Chapman et al. 2005). New studies of the kinematics of M31 dSphs (Collins et al. 2010, 2011; Kalirai et al. 2010; Tollerud et al. 2012; Chapman et al. 2013) have dramatically increased the number of systems with a measured velocity dispersion, and have shown that instead of being kinematically hotter, these systems are either very similar to, or in a number of cases (e.g., And II, And XII, And XIV, And XV, and And XXII), colder than their MW counterparts. In particular, a significant recent kinematic study of 15 M31 dSph companions using the Keck II/DEIMOS spectrograph by the Spectroscopic and Photometric Landscape of Andromeda’s Stellar Halo (SPLASH; Tollerud et al. 2012) concluded that the M31 dSph system largely obeys very similar mass–size–luminosity scalings as those of the MW. However, they also identified three outliers (And XIV, XV, and XVI) that appear to possess much lower velocity dispersions, and hence maximum circular velocities, than would be expected for these systems. Such a result suggests that there are significant differences in the formation and/or evolution of the M31 and MW dSph systems.

To investigate this further, our group has been systematically surveying the known dSphs of M31 with the Keck I/LRIS and Keck II/DEIMOS spectrographs, and have obtained kinematic data for 18 of the 28 galaxies. In this paper, we present new spectroscopic analysis for the 11 dSphs, Andromeda (And) XVII, And XVIII, And XIX, And XX, And XXI, And XXII, And XXIV, And XXV, And XXVI, the tidally disrupting And XXVII, And XXVIII, and And XXX (Cassiopeia II) using an algorithm we have developed that implements a probabilistic method of determining membership for each galaxy. In addition we re-analyze the kinematics of six dSphs that our group has previously observed (And V, VI, XI, XII, XIII, XXII) using this method with the aim of providing a homogeneous analysis of all dSphs observed by our group to date. We also provide the individual stellar velocities and properties for every star observed in our dSphs survey, allowing us to present a large catalog of stellar kinematics that will be of interest to those studying dSph systems and MW-like galaxies, whether observationally or theoretically.

The outline of this paper is as follows. In Section 2 we discuss the relevant observations, data reduction techniques. In Section 3 we outline our algorithm for the classification of member stars. In Section 4 we present an analysis of our new kinematic data sets. In Section 5 we report on the masses and densities of the dark matter halos of the M31 dSphs, comparing them to those of the MW dSphs. In Section 6 we report on the metallicities, [Fe/H], of the M31 dSphs as measured from the co-added spectra of their member stars. Finally, we conclude in Section 7.
2. OBSERVATIONS

2.1. Photometry and Target Selection

The PAndAS survey (McConnachie et al. 2009), conducted using the 3.6 m CFHT, maps out the stellar density of the disc and halo regions of the M31–M33 system over a projected area of ∼350 deg² (∼55,000 kpc²), resolving individual stars to depths of g = 26.5 and i = 25.5 with a signal-to-noise ratio (S/N) of 10, making this survey the deepest, highest resolution, contiguous map of the majority of the extended stellar halo of Andromeda galaxy to date. Each of the 411 fields in this survey (0.96 × 0.94 deg²) has been observed for at least 1350 s in both MegaCam g and i filters, in <0.8 seeing. This survey was initiated following two precursor surveys of the M31 system, the first of which surveyed the central ∼40 deg² conducted with the 2.5 m Isaac Newton Telescope (Ferguson et al. 2002; Irwin et al. 2005), and revealed a wealth of substructure in the Andromeda stellar halo, including the giant southern stream (Ibata et al. 2001). To better understand this feature, and to probe deeper into the M31 (and M33) stellar halo, a survey of the southwest quadrant of the M31 halo was initiated using the CFHT (Ibata et al. 2007), and revealed yet more substructure, including the arc-like stream Cp and Cr (Chapman et al. 2008) and a number of dwarf spheroidal satellites (Martin et al. 2006). This CFHT survey was then extended into the full PAndAS project. For details of the processing and reduction of these data, see Richardson et al. (2011). This survey has introduced us to a wealth of stellar substructure, debris and globular clusters within the Andromeda–Triangulum system. In addition, it has led to the discovery of 17 dSphs. These objects were detected in the PAndAS survey maps as over-densities in matched-filter surface density maps of metal-poor red giant branch (RGB) stars and were presented in Martin et al. (2006, 2009), Ibata et al. (2007), Irwin et al. (2008), McConnachie et al. (2008), and Richardson et al. (2011). We briefly summarize the photometric properties of all dSphs discussed within this paper in Table 1.

For the majority of these objects, the PAndAS data set formed the basis for our spectroscopic target selection. Using the color selection boxes presented in McConnachie et al. (2008), Martin et al. (2009), and Richardson et al. (2011), we isolated the RGBs of each dSph, then prioritized each star on this sequence depending on their color, i-band magnitude, and distance from the center of the dSph. Stars lying directly on the RGB, with 20.3 < i0 < 22.5 and distance, d < 4rhalf (where rhalf is the half-light radius, measured on the semi-major axis of the dSph) were highly prioritized (priority A), followed by stars on the RGB within the same distance from the center with 22.5 < i0 < 23.5 (priority B). The remainder of the mask was then filled with stars in the field with 20.3 < i0 < 23.5 and 0.5 < g − i < 4 (priority C). In general, it is the brighter, higher priority A stars that ultimately show the highest probability of membership. We also use the PAndAS photometry to help us determine membership of the dSph (discussed in Section 3).

And XXVIII is the one dSph in our sample that is not covered by the PAndAS survey. For this object, target selection followed an identical methodology to that detailed above, but used photometry from the 8th data release of the Sloan Digital Sky Survey (SDSS-III). Details of the observations and analysis of this photometry can be found in Slater et al. (2011).

2.2. Keck Spectroscopic Observations

The DEep-Imaging Multi-Object Spectrograph (DEIMOS), situated on the Nasmyth focus of the Keck II telescope is an ideal instrument for obtaining medium resolution (R ∼ 1.4 Å) spectra of multiple, faint stellar targets in the M31 dSphs. The data for the dSphs within this work were taken between 2004 September and 2012 September in photometric conditions, with typical seeing between 0.5 and 1.0. Our chosen instrumental setting covered the observed wavelength range from 5600–9800 Å and employed exposure times of 3 × 20 minute integrations. The majority of observations employed the 1200 line mm⁻¹ grating, although for four dSphs (And XI, XII, XIII, and XXIV) the lower resolution 600 line mm⁻¹ grating (R ∼ 3.8 Å FWHM) was used. The spectra from both setups typically possess S/Ns of >3 Å⁻¹ for our bright targets (i ≤ 22.0), though some of our fainter targets fall below this level. Information regarding the spectroscopic setup and observations for each dSph are displayed in Table 2.

The resulting science spectra are reduced using a custom built pipeline, as described in Ibata et al. (2011). Briefly, the pipeline identifies and removes cosmic rays, corrects for scattered light, performs flat-fielding to correct for pixel-to-pixel variations, corrects for illumination, slit function and fringing, wavelength calibrates each pixel using arc-lamp exposures, performs a two-dimensional sky subtraction, and finally extracts each spectrum—without resampling—in a small spatial region around the target. This results in a large set of pixels for each target, each of which carries a flux and wavelength (with associated uncertainties) plus the value of the target spatial profile at that pixel. We then derive velocities for all our stars with a Bayesian approach, using the CaII triplet absorption feature. Located at rest wavelengths of 8498, 8542, and 8662 Å, these strong features are ideal for determining the velocities of our observed stars. We determine the velocities by using a Markov Chain

| And V | 01:10:17.1 | +47:37:41.0 | 10.2 | 302 ± 44 | 742 ± 32 |
| And VI | 23:51:39.0 | +24:35:42.0 | 10.6 | 524 ± 49 | 783 ± 28 |
| And XI | 00:46:20.0 | +33:48:05.0 | 6.9 | 158 ± 23 | 761 ± 29 |
| And XII | 00:47:27.0 | +34:22:29.0 | 6.4 | 324 ± 56 | 928 ± 40 |
| And XIII | 00:51:50.0 | +33:00:16.0 | 6.7 | 172 ± 39 | 760 ± 126 |
| And XVII | 00:37:07.0 | +44:19:20.0 | 8.5 | 262 ± 46 | 727 ± 39 |
| And XVIII | 00:02:14.5 | +45:05:20.0 | 9.7 | 325 ± 24 | 1214 ± 43 |
| And XIX | 00:19:32.1 | +35:02:37.1 | 9.6 | 1481 ± 26 | 821 ± 43 |
| And XX | 00:07:30.7 | +35:07:56.4 | 6.3 | 114 ± 31 | 741 ± 42 |
| And XXI | 23:54:47.7 | +42:18:50.1 | 9.8 | 842 ± 77 | 827 ± 23 |
| And XXII | 01:27:40.0 | +28:05:25.0 | 6.5 | 252 ± 28 | 920 ± 39 |
| And XXIII | 00:29:21.8 | +38:43:08.0 | 10.2 | 1001 ± 52 | 746 ± 31 |
| And XXIV | 00:30:30.0 | +46:21:58.0 | 7.6 | 548 ± 35 | 898 ± 52 |
| And XXV | 00:30:08.9 | +46:51:07.0 | 9.7 | 642 ± 74 | 736 ± 49 |
| And XXVI | 00:23:56.0 | +47:54:58.0 | 7.1 | 219 ± 52 | 754 ± 38 |
| And XXVII | 00:37:27.2 | +45:23:13.0 | 7.9 | 657 ± 154 | 1255 ± 47 |
| And XXVIII | 22:32:41.2 | +31:32:51.2 | 8.5 | 210 ± 60 | 650 ± 150 |
| And XXIX | 00:36:34.9 | +49:38:48.0 | 8.0 | 267 ± 35 | 681 ± 32 |

Notes. As derived from CFHT photometry by Ibata et al. (2007), Letarte et al. (2009), Irwin et al. (2008), McConnachie et al. (2008), Martin et al. (2009), Collins et al. (2010, 2011), Brasser et al. (2011a), Richardson et al. (2011), and McConnachie (2012), updated for distances presented in Conn et al. (2012). The photometry for And VI is derived from Subaru SuprimeCam photometry (Collins et al. 2011), and the values for And XXVIII come from SDSS photometry (Slater et al. 2011).
Monte Carlo procedure where a template Ca II spectrum was cross-correlated with the non-resampled data, generating a most likely velocity for each star, and a likely uncertainty based on the posterior distribution that incorporates all the uncertainties for each pixel. Typically our velocity uncertainties lie in the range of 5–15 km s\(^{-1}\) for each pixel. While we believe this correction is robust in the high S/N regime, we argue against applying this correction in studies of Andromedean satellites, where S/N is often quite low (typically less than 8–10 Å\(^{-1}\)) for 1 hr observations of faint \((i > 21)\) RGB stars. We find that when we compute this offset for all stars within our sample, those with high S/N tend to cluster within a few km s\(^{-1}\) of the average telluric correction found for the mask. As the S/N decreases below about 10 Å\(^{-1}\), the scatter about this mean value increases dramatically, as do the uncertainties computed for each individual correction. This is because the telluric feature is a single, very broad and asymmetric feature. It is therefore easy in the noisy regime for the cross correlation routine to misalign the template and science spectrum while still producing a high confidence cross-correlation maximum.

We show this effect explicitly in the right hand panel of Figure 1 where we plot the deviation of the telluric correction for every star within our sample from the average correction determined for the spectroscopic mask it was observed with \((v_{\text{tel}} - \langle v_{\text{tel}} \rangle)\) as a function of S/N. The cyan points represent the individual data, and the large black points represent the median of all points within 1 Å bins in S/N. The error bars represent the dispersion within each bin. It is plainly seen that the median value for each bin is consistent with zero (i.e., the median), and that the dispersion increases with decreasing S/N. If we were to apply these velocity corrections to all our stars, it is probable that we would merely increase the velocity uncertainties rather than reducing them.

For this reason, we take a different approach. Using solely the telluric velocity corrections of stars from each observed mask whose spectra have S/N > 7, we measure (1) the average telluric correction for the mask and (2) the evolution of the telluric correction as a function of mask position. In this way, we can track any gradient in our measurements that could be caused by, e.g., rotational offsets in our mask. In general, we find these corrections to be slight. The average measured offset across all our masks is 3.8 km s\(^{-1}\) (ranging from between –3.4 km s\(^{-1}\) and

### Table 2

| Object | Date       | Instrument | Grating | Res. | \(\sigma_{v,2000}\) | \(\delta_{v,2000}\) | P.A. | Exp. (s) | N\(_{\text{Tag}}\) | N\(_{\text{Mem}}\) |
|--------|------------|------------|---------|------|----------------|----------------|------|----------|----------------|----------------|
| And V  | 2009 Aug 16| LIRIS      | 831/8200| 3.0 Å| 01:10:18.21    | +47:37:53.3 | 0°   | 3600     | 50            | 15             |
| And VI | 2009 Sep 17–19| DEIMOS | 1200   | 1.3 Å| 23:51:51.49    | +24:34:57.0 | 0°   | 5400     | 113           | 43             |
| And XI | 2006 Sep 23| DEIMOS | 600    | 3.5 Å| 00:46:28.08    | +33:46:28.8 | 0°   | 3600     | 33            | 5              |
| And XII| 2006 Sep 21–23| DEIMOS | 600    | 3.5 Å| 00:47:32.89    | +34:22:26.8 | 0°   | 3600     | 49            | 8              |
| And XIII| 2006 Sep 23| DEIMOS | 600    | 3.5 Å| 00:52:00.22    | +32:59:16.2 | 0°   | 3600     | 46            | 4              |
| And XVII| 2011 Sep 26| DEIMOS | 1200   | 1.3 Å| 00:37:51.09    | +44:17:51.9 | 280° | 3600     | 149           | 8              |
| And XVIII| 2010 Sep 9| DEIMOS | 1200   | 1.3 Å| 00:02:14.50    | +45:05:20.0 | 90°  | 3600     | 73            | 4              |
| And XIXa| 2011 Sep 26| DEIMOS | 600    | 3.5 Å| 00:19:45.04    | +35:05:28.8 | 270° | 3600     | 107           | 15             |
| And XIXb| 2011 Sep 26| DEIMOS | 1200   | 1.3 Å| 00:19:30.88    | +35:07:34.1 | 0°   | 3600     | 108           | 9              |
| And XX  | 2010 Sep 9| DEIMOS | 1200   | 1.3 Å| 00:07:30.69    | +35:08:02.4 | 90°  | 3600     | 85            | 4              |
| And XXI | 2011 Sep 26| DEIMOS | 1200   | 1.3 Å| 23:54:47.70    | +24:28:33.6 | 180° | 3600     | 157           | 32             |
| And XXIIa| 2009 Sep 23| DEIMOS | 1200   | 1.3 Å| 01:27:52.37    | +28:05:22.3 | 90°  | 1200     | 93            | 4              |
| And XXIIb| 2010 Sep 10| DEIMOS | 1200   | 1.3 Å| 01:27:52.37    | +28:05:22.3 | 0°   | 3600     | 73            | 6              |
| And XXIIla| 2010 Sep 9| DEIMOS | 1200   | 1.3 Å| 01:29:18.18    | +38:43:50.4 | 315° | 3600     | 196           | 24             |
| And XXIIlb| 2010 Sep 10| DEIMOS | 1200   | 1.3 Å| 01:29:21.87    | +38:44:58.7 | 245° | 3600     | 189           | 18             |
| And XXIVa| 2010 Sep 9| DEIMOS | 1200   | 1.3 Å| 01:18:32.90    | +46:22:50.0 | 30°  | 3600     | 192           | 1              |
| And XXIVb| 2011 May 31| DEIMOS | 600    | 3.5 Å| 01:18:32.90    | +46:22:50.0 | 0°   | 2700     | 115           | 11             |
| And XXV | 2010 Sep 10| DEIMOS | 1200   | 1.3 Å| 00:30:01.88    | +46:50:31.0 | 90°  | 3600     | 183           | 26             |
| And XXVI| 2010 Sep 10| DEIMOS | 1200   | 1.3 Å| 00:23:41.42    | +47:54:56.8 | 90°  | 3600     | 179           | 6              |
| And XXVII| 2010 Sep 10| DEIMOS | 1200   | 1.3 Å| 00:37:31.93    | +45:23:55.4 | 45°  | 3600     | 131           | 8              |
| And XXVIII| 2012 Sep 21| DEIMOS | 1200   | 1.3 Å| 22:32:32.71    | +31:13:13.2 | 140° | 3600     | 102           | 17             |
| Cass II | 2011 Sep 28| DEIMOS | 1200   | 1.3 Å| 00:37:00.84    | +49:39:12.0 | 270° | 3600     | 156           | 8              |
+10.6 km s$^{-1}$). The measured gradients are very slight, resulting in an average end-to-end mask difference of 2.6 km s$^{-1}$, with a range of 0.1–7.2 km s$^{-1}$, typically within our measured velocity uncertainties.

### 3. A PROBABILISTIC DETERMINATION OF MEMBERSHIP

Determining membership for Andromedean dwarf spheroidals is notoriously difficult in the best of cases. We only possess information about the velocity, color–magnitude diagram (CMD) position, distance from the center of the dSph, and spectroscopic metallicity (although this carries large uncertainties of >0.3 dex for individual stars). Depending on the systemic velocity of the dSph, we must try to use these properties to distinguish the likely members from either MW halo K-dwarfs ($v_{\text{hel}} \gtrsim -150$ km s$^{-1}$) or M31 halo giants ($v_{\text{halo}} \approx -300$ km s$^{-1}$, $\sigma_{v,\text{halo}} \approx 90$ km s$^{-1}$; Chapman et al. 2006). In the case of Galactic contamination, our spectra also cover the region of the Na I doublets ($\sim$8100 Å). As this feature is dependent on the stellar surface gravity, it is typically stronger in dwarf stars than in giants. However, there is a significant overlap between the two, especially in the CMD color region of interest for Andromedean RGB stars. In the past, groups have focused on making hard cuts on likely members in an attempt to weed out likely contaminants (e.g., based on their distance from the center of the galaxy or their velocity; Chapman et al. 2005; Collins et al. 2010, 2011; Kalirai et al. 2010), but such “by eye” techniques are not particularly robust. Tollerud et al. (2012, hereafter T12) recently presented an analysis of a number of M31 dSphs where they used a more statistical method to ascertain likely membership, using the distance from the center of, and position in the CMD of stars targeted within their DEIMOS masks. Here we employ a similar technique that will assess the probability of stars being members of a dSph based on (1) their position on the CMD; (2) their distance from the center of the dSph and, in addition; (3) their position in velocity space, giving the likelihood of membership as

$$P_i \propto P_{\text{CMD}} \times P_{\text{dist}} \times P_{\text{vel}}.$$  \hspace{1cm} (1)

Below, we fully outline our method, and implement a series of tests to check it can robustly recover the kinematics of the M31 dSphs.

#### 3.1. Probability Based on CMD Position, $P_{\text{CMD}}$

For the first term, $P_{\text{CMD}}$, we are interested in where a given star observed in our mask falls with respect to the RGB of the observed dSph. T12 use the distance of a given star from a fiducial isochrone fit to the dwarf photometry to measure this probability. Here, we determine this value from the data itself, rather than using isochrones. Using the PAndAS CFHT photometry, we construct a normalized Hess diagram for the central region (i.e., within $2 \times r_{\text{halo}}$) of the dSph, and one of a surrounding “field” comparison region. By combining these two Hess diagrams, we can then map both the color distribution of the dSph and that of our contaminating populations. We use both directly as probability maps, where the densest region would have a value of 1.

So that we are not dominated by shot noise of sparsely populated regions of the CMD, we use only the region of the RGB. We do this by assigning a generous bounding box around the RGB as seen in the left hand panel of Figure 2 where we display the PAndAS CMD for the well populated And XXI RGB. We have zoomed in on the region for which DEIMOS observations with reliable velocities can be obtained, e.g., $i < 23.5$. The bounding box is shown with red dashed...
The half-light radii of all these objects are known and can be easily determined from the known radial profile of the dSphs. For an analysis of these stars (selecting out any obvious substructures and the Andromedean disc) we find that the M31 halo is well approximated by a single Gaussian with a systemic velocity of \( v_{r,\text{halo}} = -308.8 \text{ km s}^{-1} \) and \( \sigma_{v,\text{halo}} = 96.3 \text{ km s}^{-1} \), giving a probability density function for a given star with a velocity \( v_r \) and velocity uncertainty of \( \sigma_{v,r} \) of

\[
P_{\text{halo}} = \frac{1}{\sqrt{2\pi}(\sigma_{v,\text{halo}} + \sigma_{v,r})} \exp \left[ -\frac{1}{2} \left( \frac{v_r - v_{r,\text{halo}}}{\sqrt{\sigma_{v,\text{halo}}^2 + \sigma_{v,r}^2}} \right)^2 \right].
\]  

\( (4) \)

The MW halo population is well approximated by two Gaussians with \( v_{r,\text{MW1}} = -81.2 \text{ km s}^{-1}, \sigma_{v,\text{MW1}} = 36.5 \text{ km s}^{-1} \) and \( v_{r,\text{MW2}} = -40.2 \text{ km s}^{-1} \) and \( \sigma_{v,\text{MW2}} = 48.5 \text{ km s}^{-1} \), resulting in a probability density function for a given star with a velocity \( v_r \) and velocity uncertainty of \( \sigma_{v,r} \) of

\[
P_{\text{MW}} = \frac{R}{\sqrt{2\pi}(\sigma_{v,\text{MW1}} + \sigma_{v,r})} \exp \left[ -\frac{1}{2} \left( \frac{v_r - v_{r,\text{MW1}}}{\sqrt{\sigma_{v,\text{MW1}}^2 + \sigma_{v,r}^2}} \right)^2 \right] + \frac{1 - R}{\sqrt{2\pi}(\sigma_{v,\text{MW2}} + \sigma_{v,r})} \exp \left[ -\frac{1}{2} \left( \frac{v_r - v_{r,\text{MW2}}}{\sqrt{\sigma_{v,\text{MW2}}^2 + \sigma_{v,r}^2}} \right)^2 \right],
\]  

\( (5) \)

Figure 2. Left: the PAndAS CMD for And XXI, showing all stars within 2 \( r_{\text{half}} \) of the dwarf center. The red dashed lines show the bounding box we use to construct our probability map for the RGB of the dSph. Right: a background normalized Hess diagram for the RGB region of And XXI. The color represents the probability, \( P_{\text{CMD}} \) in each cell for a star in that position belonging to And XXI. This diagram is used as a probability map for all our spectroscopically observed stars. Red points represent stars DEIMOS stars for which \( P_{\text{CMD}} \gtrsim 10^{-6} \), while the blue stars represent objects for which \( P_{\text{CMD}} \lesssim 10^{-6} \).

(A color version of this figure is available in the online journal.)
where $R$ is the fraction of stars in the first MW peak, and $(1 - R)$ is the fraction of stars in the second peak. The value of $R$ is determined empirically from our DEIMOS data set.

A strong kinematic peak outside of these two populations can then be searched for using a maximum likelihood technique, based on the approach of Martin et al. (2007). We search for the maximum in the likelihood function that incorporates the two contamination populations plus an additional Gaussian structure with systemic velocity $v_{r,\text{substr}}$ and a dispersion of $\sigma_{v,\text{substr}}$, defined as

$$P_{\text{substr}} = \frac{1}{\sqrt{2\pi(\eta^2\sigma_v^2 + \sigma_{v,i}^2)}} \times \exp \left[ -\frac{1}{2} \left( \frac{v_{r,\text{substr}} - v_{r,i}}{\sqrt{\eta^2\sigma_v^2 + \sigma_{v,i}^2}} \right)^2 \right].$$  \hspace{1cm} (6)

Here, to ensure that we have not biased our $P_{\text{substr}}$ strongly against stars that lie within the wings of the Gaussian distribution of dwarf spheroidal velocities, we have included a multiplicative free parameter, $\eta$, to our derived value of $\sigma_v$. To determine the ideal value of $\eta$, we ran our algorithm over all our data sets, changing the value of $\eta$ from 0.5–10.5 to see its effect on the final derived systemic velocities and velocity dispersion. We find that in all cases, the solutions converge at values of $\eta \sim 2–4$. For dSphs whose kinematics are well separated from contaminants, the derived kinematics can remain stable up to much larger values of $\eta$, however for those with systemic velocities within the velocity regime of the MW, the solution quickly destabilizes as more contaminants are included as probable members. We show this implicitly in Figure 3, where we present the effect of modifying $\eta$ on six dSphs, And XII, XIX, XXI, XXII, XXIII, and XXV. These objects were selected as they nicely probe our data sets with low numbers of probable member stars ($\sim$8), to those where we have tens of probable members, as well as sampling dSphs from highly contaminated to well isolated kinematic regimes. The value of $\eta$ is therefore independently determined for each data set separately, and we report its final value in Table 4.

$$P_{\text{substr}} = \frac{1}{\sqrt{2\pi(\alpha^2\sigma_v^2 + \sigma_{v,i}^2)}} \times \exp \left[ -\frac{1}{2} \left( \frac{v_{r,\text{substr}} - v_{r,i}}{\sqrt{\alpha^2\sigma_v^2 + \sigma_{v,i}^2}} \right)^2 \right].$$  \hspace{1cm} (7)

The likelihood function can then be simply written as

$$\log[L(v_r, \sigma_v)] = \sum_{i=1}^{N} \log(\alpha P_{v,\text{halo}} + \beta P_{v,\text{MW}} + \gamma P_{v,\text{substr}}),$$  \hspace{1cm} (8)

where $\alpha$, $\beta$, and $\gamma$ represent the Bayesian priors, i.e., the expected fraction of stars to reside in each population. These are determined by starting with arbitrary fractions (for example, 0.2, 0.5, and 0.3, respectively) and are then adjusted to the posterior distribution until priors and posteriors match. This technique will therefore identify an additional kinematic peak, independent of the MW and M31 halo populations, if it exists. We stress that these are not the final systemic velocity and dispersion of the dSph, but merely indicate a region in velocity space in which an excess of stars above the two contaminant populations is seen. In Figure 4, we show the result of this process for the And XXI dSph. Here, the substructure is clearly visible as a cold spike at $\sim -400 \text{ km s}^{-1}$.

Now that we have a velocity profile for our three components (MW, M31 halo, and the dSph), we can assign probabilities for each star within our sample belonging to each population using simple Bayesian techniques, i.e., the probability that a given star belongs to the substructure, $P_{\text{vel}}$, is

$$P_{\text{vel}} = \frac{\nu P_{\text{substr}}}{\alpha P_{\text{halo}} + \beta P_{\text{MW}} + \gamma P_{\text{substr}}}$$  \hspace{1cm} (9)

and the probability of being a contaminant is

$$P_{\text{vel}} = \frac{\alpha P_{\text{halo}} + \beta P_{\text{MW}}}{\nu P_{\text{substr}}}. \frac{\gamma P_{\text{halo}}}{\nu P_{\text{substr}}}.$$  \hspace{1cm} (10)

3.4. Measuring $v_r$ and $\sigma_v$

Upon applying this to our data, we can identify the most probable members of each dSph, without having to apply any additional constraints or cuts.

Having established the membership probability for each observed star (as detailed above) we now calculate the kinematic properties of each dSph; namely their systemic velocities ($v_r$) and velocity dispersions ($\sigma_v$). We use the maximum likelihood technique of Martin et al. (2007), modified to include our probability weights for each star. We sample a coarse grid in ($v_r, \sigma_v$) space and determining the parameter values that maximize the likelihood function (ML), defined as

$$\log[L(v_r, \sigma_v)] = -\frac{1}{2} \sum_{i=1}^{N} \log \left[ \frac{1}{\nu P_{\text{halo}} + \beta P_{\text{MW}} + \gamma P_{\text{substr}}} \right] \sum_{i=1}^{N} \log \left[ \frac{1}{\nu P_{\text{halo}} + \beta P_{\text{MW}} + \gamma P_{\text{substr}}} \right]$$  \hspace{1cm} (11)

where $N$ is the number of stars in the sample, $v_{r,i}$ is the radial velocity measured for the $i$th star, $\sigma_{v,i}$ is the corresponding uncertainty, and $\sigma_{\text{tot}} = \sqrt{\sigma_v^2 + \sigma_{v,i}^2}$. In this way, we aim to separate the intrinsic dispersion of a system from the dispersion introduced by the measurement uncertainties.

3.5. Testing Our Probabilistic Determination of Membership and Calculations of Kinematic Properties

Having developed the above technique, it is important for us to rigorously test that it is robust enough to accurately determine the global kinematic properties for each of our data sets. In Appendix A, we examine in detail a number of potential issues that could cause our algorithm to return biased or incorrect results. These are the inclusion of a velocity dependent term in our probability calculation, the effect of including low S/N data (S/N < 5 Å) in our analysis and the effect of small sample sizes ($N_s < 8$) on our measurements of kinematic properties. We briefly summarize our findings here, and refer the reader to Appendix A for a more detailed description.

This work has introduced the concept of assigning a probability of membership for a given star to a dSph based on the prior knowledge of the velocity profiles of our expected contaminant populations, $P_{\text{vel}}$, a technique that has not previously been used in the study of M31 dSphs. To test that this is not biasing our results, we can simply remove this term from Equation (1).
and follow the technique of T12, where they use only \( P_{\text{CMD}} \) and \( P_{\text{dist}} \) terms and then cut all stars with \( P_i < 0.1 \) and velocities that lie greater than \( 3\sigma \) from the mean of this sample from their final analysis. We find that both techniques produce very similar results; however, our algorithm is more robust in regimes where the systemic velocity of the dSph is close to that of the MW, and in dSphs where our number of probable member stars is low (\( N^* < 10 \)).

To test the effect of low S/N data on our calculations of \( v_r \) and \( \sigma_v \), we use our data sets for And XXI, XXIII, and XXV, all of which have \( \geq 25 \) associated members. For each data set, we apply a series of cuts to the sample based on S/N (at levels of S/N > 2, 3, 4, and 5 Å) and rerun our algorithm. In all cases we find that the derived probabilities do not significantly differ when the low S/N data are included, justifying our inclusion of all stars for which velocities are calculated by our pipeline.

We also test the ability of our algorithm to measure \( v_r \) and \( \sigma_v \) in the small \( N^* \) regime. For some of our data sets, we are only able to identify a handful of stars as probable members. In theory, one can calculate velocity dispersions accurately from only three stars if one is confident of ones measurement uncertainties, as is demonstrated by Aaronson (1983) measurement of the velocity dispersion for Draco from only three stars, which remains consistent with modern day measurements from significantly larger data sets (Walker et al. 2009b). We can test if our results are similarly robust using our larger data sets (such as And XXI, XXIII, and XXV) by randomly selecting 4, 6, 8, 10, 15, 20, and 25 stars from these data sets and rerunning our algorithm to

---

**Figure 3.** The effect of modifying \( \eta \)—a multiplicative weight applied to the dispersion of the identified substructure in our \( P_{\text{vel}} \) term—on the final derived systemic velocities (\( v_r \)) and dispersions (\( \sigma_v \)) for six of our dSphs. The effect of increasing \( \eta \) is typically more pronounced in objects with systemic velocities close to that of MW contamination (such as And XIX and XXV) than for other objects. Dashed lines represent the optimal value of \( \eta \) for each system.

(A color version of this figure is available in the online journal.)
Figure 4. A velocity histogram for all observed stars in the field of And XXI. Our empirical Gaussian fits to the full Keck II data set for the M31 and MW halos are overlaid in blue and green, respectively. A cold, kinematic peak at $-400 \, \text{km} \, \text{s}^{-1}$ is also seen, and this is the likely signature of the dSph. Our coarse, initial ML procedure identifies this peak, and the values of $v_{\text{sys}}$ and $\sigma_v$ it measures are used to derive our kinematic probability, $P_{\text{vel}}$.

(A color version of this figure is available in the online journal.)

determine $v_r$ and $\sigma_v$ from these subsets. We repeat this exercise 1000 times for each sample size, and examine the mean and standard deviations for the computed quantities. We find that on average, for all sample sizes, our routine measures systemic velocities and velocity dispersions that are entirely consistent with those measured from the full sample, with a spread that is very comparable to typical errors produced by our ML routine in these low $N_*$ regimes. As such, we conclude that our technique is able to place sensible limits on these values, even when dealing with as few as four member stars.

Finally, as the individual positions, velocities and velocity uncertainties for all the stars analyzed in T12 are publicly available (with the data from the non-member stars having been kindly passed on to us by the SPLASH team), we can check that our algorithm is able to reproduce the values they measure for their M13 dSph sample. We find that, in all cases, we calculate systemic velocities and velocity dispersions that agree with their measured values to well within their 1$\sigma$ uncertainties.

These tests demonstrate that our method is robust enough to accurately determine the global kinematic properties of M31 dSphs across a wide range of sample sizes and data quality. We therefore proceed to apply it to the data sets of all of the dSphs for which our group has acquired Keck II/DEIMOS observations to date.

4. THE KINEMATICS OF M31 dSphs

With this vast data set of dSph kinematics now in hand, we can begin to statistically probe their structures more fully. In Figure 5 we display a summary of the velocities and positions of 26 of the 28 dSphs for which kinematic data are available.

(A color version of this figure is available in the online journal.)

Figure 5. Positions of 26 of the 28 Andromeda dSphs, color coded by their heliocentric velocity, $v_r$ (taken from this work, Kalirai et al. 2010, and T12). The solid line represents the PAndAS survey footprint. M31 is shown by the double ellipse, where the outer ellipse shows a segment of a 55 kpc radius ellipse flattened to $c/a = 0.6$, and the major-axis and minor-axis are indicated with straight lines out to this ellipse. The inner ellipse corresponds to a disc of radius $2^\circ$ (27 kpc), with the same inclination as the main M31 disc. M33 is shown as a singular ellipse.

(A color version of this figure is available in the online journal.)
where the values are taken from this work, T12, and Kalirai et al. (2010). In the following sections, we will discuss the individual stellar kinematics, masses, and chemistries of the dSphs analyzed within this work.

4.1. Andromeda XVII

And XVII was discovered by Irwin et al. (2008), and it is located at a projected distance of \( \sim 40 \) kpc to the northwest of Andromeda. A detailed study of deep imaging obtained with the Large Binocular Camera on the Large Binocular Telescope (LBT) was also performed by Brasseur et al. (2011b), and throughout, we use the structural properties as determined from this work. It is a faint, compact galaxy \( (M_V = -8.61, r_{\text{half}} = 1.24 \text{ or } 262^{+53}_{-46} \text{ pc}) \). In the left panel of Figure 6 we display the PAndAS CMD for And XVII. Overplotted we show the observed DEIMOS stars, color-coded by their probabilities of membership. The open symbols represent stars for which
$P_i < 10^{-6}$. We employ this cut solely to clarify which stars have the highest probability of belonging to And XVII. In the right hand panel, we display the basic kinematic information for And XVII. In the top panel of this subplot, we show a velocity histogram for all stars observed within the LRS mask, and stars with $P_i > 10^{-6}$ are highlighted with a filled red histogram. The center panel shows the velocities as a function of distance from the center of And XVII (and the red dashed lines indicate 1, 2, 3, and $4 \times r_{\text{half}}$), and the lower panel shows the photometric metallicities for all stars, as determined using Dotter et al. (2008) CFHT isochrones. Again, all points are color-coded by their probability of membership. Finally, the two lower panels show the resulting, one-dimensional, probability-weighted, marginalized maximum likelihood distributions for $v_r$ and $\sigma_v$ for this data set. From the kinematics presented in Figure 6, which represent the first spectroscopic observations of this object, we see the signature of the dwarf galaxy as a cold spike at $v_r \sim -250 \text{ km s}^{-1}$. From the lower panels of this figure and the accompanying CMD we see that there is a cluster of seven stars sitting within this spike that are centrally concentrated and are consistent with the RGB of the dwarf itself, leading us to believe that our algorithm has cleanly detected the signature of the galaxy. Interestingly, we also see three stars that, kinematically, are indistinguishable from the stars that have been dubbed as probable members in our analysis. However, they all sit at large distances from the center of And XVII, equivalent to greater than six times the half-light radius of the dwarf, and hence the routine has classified them as likely members of the M31 halo rather than And XVII members. But, given their tight correlation in velocity to the systemic velocity of And XVII the possibility exists that these are extra-tidal stars of And XVII. No sign of extra-tidal features were cited in either the discovery paper of And XVII or the LBT follow up, but given its position in the north M31 halo where contamination from the MW becomes increasingly problematic, and its relatively low luminosity ($M_V = -8.5$), such features may be difficult to see within the imaging. However, at present they are considered unlikely members by our routine, and do not factor into our calculation of global kinematic properties for this object. We find $v_r = -251.6^{+1.8}_{-2.0} \text{ km s}^{-1}$ and $\sigma_v = 2.9^{+2.2}_{-1.9} \text{ km s}^{-1}$.

4.2. Andromeda XVIII

Andromeda XVIII (And XVIII) was detected by McConnachie et al. (2008) in the PAndAS CFHT maps. Located at a projected distance of $\sim 110$ kpc to the northwest of M31, it is one of the most distant of its satellites, sitting $\sim 600$ kpc behind the galaxy, making spectroscopic observations of its individual RGB stars taxing, as they are all relatively faint ($i \gtrsim 22.2$). Thus, from our 1 hr DEIMOS observation, we were only able to confirm four stars as probable members (see Figure 7). We determine the global systemic velocity to be $v_r = -346.8 \pm 2.0 \text{ km s}^{-1}$, and we are unable to resolve a velocity dispersion, finding $\sigma_v = 0.0^{+2.7}_{-0.0} \text{ km s}^{-1}$ where the upper bound is determined from the formal 1$\sigma$ confidence interval produced by our maximum likelihood analysis. This suggests that the four stars we are able to confirm as members do not adequately sample the underlying velocity profile. The systemic velocity we measure is different to that presented in T12 of $v_r = -332.1 \pm 2.7$ at a level of 3.4$\sigma$. Our 1$\sigma$ limit of 2.7 km s$^{-1}$ is also at odds with the dispersion determined by T12 ($\sigma_v = 9.7 \pm 2.3$). They were able to measure velocities for significantly more probable member stars (22 versus 4) owing to their longer integration of 3 hr. The faintness of our targets and shorter exposure time could mean that strong sky absorption lines have systematically skewed our velocity measurements for these stars, and this could explain the discrepancy of our measurements with respect to those of T12. To check against this, we again perform weighted cross-correlations to each of the three Ca ii lines individually. We find that the values we obtain, and their average, are fully consistent with that derived from the technique described in Section 2.2, differing by less than 3 km s$^{-1}$ from those values. The true systemic velocity of And XVIII therefore remains unclear. However, given their larger sample size, the T12 systemic properties are more statistically robust than those we present here.

4.3. Andromeda XIX

Andromeda XIX (And XIX) was first reported in McConnachie et al. (2008), and is a relatively bright, very extended ($M_V = -9.3$, $r_{\text{half}} = 1.5$ kpc) dSph, located at a projected distance of $\sim 180$ kpc to the southwest of M31. Its unusual morphology, very low surface brightness $\Sigma_r = 30.2$ mag arcsec$^{-2}$, and evidence in the photometry for a possible link to the major axis substructure reported in Ibata et al. (2007) caused McConnachie et al. (2008) to question whether And XIX was truly a dynamically relaxed system, or whether it had experienced a significant tidal interaction. Here, we present the first spectroscopic observations of the And XIX satellite in Figure 8 from two DEIMOS masks placed at different position angles. These data allow us to comment on its dark matter content, and on the likelihood of a tidal origin for its unique structure. We identify 27 stars where $P_i > 10^{-6}$ within the system. These measurements were made increasingly challenging as the systemic velocity we measure is $v_r = -111.6^{+1.6}_{-1.3} \text{ km s}^{-1}$, placing it within the regime of Galactic contamination. However, we are confident that our algorithm is robust to this unfortunate location of And XIX in velocity space (see discussion in Section 3.5 and Appendix A). As a further check that none of the stars we define as probable members are actually foreground contaminants, we measure the equivalent widths (EWs) of the Na i doublet lines (located at $\sim 8100$ Å). These gravity-sensitive absorption lines are typically significantly stronger in foreground dwarf stars than M31 RGB stars, although there is some overlap between the two populations. For the stars tagged as probable members by our algorithm, we find no evidence of strong absorption in the region of the Na i doublet, and are confident that our algorithm is robust to this unfortunate location of And XIX in velocity space. However, given the relatively cold velocity dispersion for this object of $\sigma_v = 4.7^{+1.6}_{-1.4} \text{ km s}^{-1}$, which is surprising given the radial extent of this galaxy. This result will be discussed further in Section 5.1, and in a follow-up paper (M. L. M. Collins et al., in preparation).

4.4. Andromeda XX

And XX was the third of three dSphs discovered by McConnachie et al. (2008), and is notable for being one of the faintest dSph companions detected surrounding Andromeda thus far. With $M_V = -6.3$ and $r_{\text{half}} = 114^{+31}_{-12}$ pc, it is a challenging object to study spectroscopically as there are very few stars available to target on its RGB, as shown in the top left subplot in Figure 9. As a result, our algorithm is only able to find four stars for which $P_i > 10^{-6}$. These are found to cluster around $v_r = -456.2^{+3.3}_{-3.2}$ km s$^{-1}$, with a dispersion of $\sigma_v = 7.1^{+3.2}_{-2.0}$ km s$^{-1}$. Despite the low number of stars, we are confident in this detection, as the systemic velocity places it in the outer wings of the velocity profile of the M31 halo. And XX is
also located at a large projected distance from M31 of ∼130 kpc, where we expect the density of the M31 halo to be very low. As such, seeing four halo stars so tightly correlated in velocity in the wings of the halo velocity profile within such a small area of the sky (all stars are within 1′ of the center of And XX) is highly unlikely. We caution the reader that, while we are confident that our algorithm is able to measure velocity dispersions for sample sizes as small as four stars, as we are not probing the full velocity profile of this object this measurement ideally needs to be confirmed with larger numbers of member stars.

4.5. Andromeda XXI

Andromeda XXI (And XXI) was identified within the PAndAS imaging maps by Martin et al. (2009). It is a relatively bright dSph ($M_V = -9.9$), located at a projected distance of ∼150 kpc from M31, and it has a half-light radius of $r_{\text{half}} = 842 \pm 77$ pc. We present our spectroscopic observations for this object in Figure 10, and in the top right subplot, we can clearly see the signature of And XXI as a cold spike in velocity with 32 probable member stars, located at $v_r = -362.5 \pm 0.9$ km s$^{-1}$, with a curiously low velocity dispersion of only $\sigma_v = 4.5_{-1.3}^{+1.0}$ km s$^{-1}$. These results are completely consistent with those of T12, where they measured $v_r = -361.4 \pm 5.8$ km s$^{-1}$ and $\sigma_v = 7.2 \pm 5.5$ km s$^{-1}$. As their sample contained only 6 likely members compared with the 29 we identify here, ours constitute a more statistically robust measurement of the global kinematics for this object than those presented in T12.

4.6. Andromeda XXII

Andromeda XXII (And XXII) was identified within the PAndAS imaging maps by Martin et al. (2009), and is a
relatively faint dSph, with $M_V = -6.5$. Its physical position in the halo, located at a distance of 224 kpc in projection from M31, but only 42 kpc in projection from M33, led the authors to postulate that it could be the first known dSph satellite of M33. Subsequent work analyzing the kinematics of And XXII by T12 measured a systemic velocity for And XXII of $-126.8 \pm 3.1$ km s$^{-1}$ from seven stars, more compatible with the systemic velocity of M33 ($-178$ km s$^{-1}$; Mateo 1998) than that of M31. Another study by Chapman et al. (2013) using the same data and the same method we present here concluded the same, measuring a systemic velocity for the satellite of $-129.8 \pm 2.0$ km s$^{-1}$ from 12 probable member stars, consistent with the T12 value. Chapman et al. (2013) also compare the position and kinematics of And XXII with a suite of $N$-body simulations of the M31–M33 system, concluding that And XXII was a probable M33 satellite.

In Figure 11, we present the same data as analyzed by Chapman et al. (2013) for completeness. The velocity dispersion of And XXII is just resolved at $\sigma_v = 2.8^{+1.9}_{-1.4}$ km s$^{-1}$, completely consistent with the value of $\sigma_v = 3.5^{+4.2}_{-2.5}$ km s$^{-1}$ from T12. As our values are calculated from a 50% greater sample size, we posit that they are the more statistically robust.

4.7. Andromeda XXIII

Andromeda XXIII (And XXIII) was the first of five M31 dSphs identified by Richardson et al. (2011). Located at a projected distance of $\sim 130$ kpc to the east of Andromeda, it is relatively bright, with $M_V = -10.2$, and extended, with
$r_{\text{half}} = 1001^{+53}_{-52}$ pc. Our routine clearly detects a strong cold kinematic peak for And XXIII located around $-230$ km s$^{-1}$ and calculates a systemic velocity of $v_r = -237.7 \pm 1.2$ km s$^{-1}$, and a velocity dispersion of $\sigma_v = 7.1 \pm 1.0$ km s$^{-1}$ from 40 probable member stars, as show in Figure 12. This small, positive velocity relative to M31, combined with its large projected distance from the host suggests that And XXIII is not far past the apocenter of its orbit, heading back toward M31.

4.8. Andromeda XXIV

And XXIV was also first reported in Richardson et al. (2011). Relatively faint and compact ($M_V = -7.6$, $r_{\text{half}} = 548^{+37}_{-37}$ pc), spatially it is located $\sim 200$ kpc from M31, along its northern major axis. And XXIV was observed on two separate occasions as detailed in Table 2. For the first mask, there was an error in target selection, and as a result, only one star that lay on the RGB of And XXIV was observed. The second mask was observed in 2011 May, however owing to target visibility, only a short integration of 45 minutes was obtained, which resulted in higher velocity uncertainties than typically expected ($\sim 8$ km s$^{-1}$ versus $\sim 5$ km s$^{-1}$). For this reason, we have only included stars from this mask with $i < 22.0$, as the spectra for fainter stars were too noisy to determine reliable velocities from. The systemic velocity of And XXIV also unsatisfactorily coincides with that of the MW halo contamination, as can be seen in Figure 13.

Figure 9. As Figure 6, but for And XX.

(A color version of this figure is available in the online journal.)
As for And XIX, we check the strength of the Na\textsc{i} doublet of all the stars classified as potential members for And XXIV, and find no significant absorption, making them unlikely foreground contaminants. But, given the lower quality of this data set, this check is far from perfect, and it is possible that we have included contaminants from the MW within our sample. Owing to the larger velocity uncertainties of the And XXIV data set, and the overlap of And XXIV with the MW, the determination of probability of membership for stars within this data set is based largely on their position in the CMD (e.g., location on the RGB) and their distance from the center of And XXIV.

When we run our machinery over the data acquired from both masks, we identify only three probable members and determine a systemic velocity of $v_r = -128.2 \pm 5.2$ km s$^{-1}$ and we resolve a velocity dispersion of $\sigma_v = 0.0^{+7.3}_{-1}$ km s$^{-1}$. Given the lower quality of this data set in comparison to the remainder of those we present in this work, and the overlap of And XXIV in velocity space with contamination from the MW, a robust kinematic detection and characterization of this galaxy is made incredibly challenging. As such, we present these results as a tentative identification of And XXIV, and do not include its measured properties in the remainder of our analysis. Further kinematic follow-up of And XXIV is required to understand this system. We present the velocities of all bright stars for which velocity measurements were possible in Table 3 so that they may be helpful for any future kinematic analysis of this system.

Figure 10. As Figure 6, but for And XXI.

(A color version of this figure is available in the online journal.)
**Figure 11.** As Figure 6, but for And XXII.

(A color version of this figure is available in the online journal.)

**Table 3**
Details of Probable dSph Members

| Field | Star ID | $a_{0,2000}$ | $d_{0,2000}$ | $g$ | $i$ | $v_{hel}$ | $v_{err}$ | S/N | $P_i$ |
|-------|---------|--------------|--------------|-----|-----|-----------|-----------|-----|-----|
| And V | 9       | 1:10:2.38    | 47:37:48.5   | 23.640 | 22.402 | -371.270 | 5.080 | 1.700 | 0.014 |
| And V | 12      | 1:10:5.540   | 47:36:41.6   | 23.100 | 21.530 | -406.500 | 3.600 | 2.000 | 0.111 |

(This table is available in its entirety in a machine-readable form in the online journal. A portion is shown here for guidance regarding its form and content.)
4.9. Andromeda XXV

And XXV was identified in Richardson et al. (2011) as a relatively bright ($M_V = -9.7$), extended ($r_{\text{half}} = 642^{+17}_{-74}$ pc) dwarf spheroidal, located at a projected distance of $\sim 90$ kpc to the northwest of M31. As with And XXIII, we present here a kinematic analysis of And XXV. The results are displayed in Figure 14. We see that the systemic velocity of And XXV ($v_r = -107.8 \pm 1.0$ km s$^{-1}$), places it in the regime of the Galactic foreground. However, given the strong over-density of stars with this velocity relative to the expected contribution of MW stars, we are confident that our routine has detected 25 likely members for this object. We check the strength of the Na I doublet in these likely members, and find no significant absorption, making them unlikely foreground contaminants. As for And XIX and XXI, we find that And XXV has a curiously low velocity dispersion for its size, with $\sigma_v = 3.0^{+1.1}_{-1.0}$ km s$^{-1}$. We discuss the significance of this further in Section 5.1 and M. L. M. Collins et al. (2013, in preparation).

4.10. Andromeda XXVI

And XXVI is a relatively faint ($M_V = -7.1$) dSph with $r_{\text{half}} = 219^{+67}_{-52}$ pc, also first reported in Richardson et al. (2011). Its low luminosity makes observing large numbers of member stars difficult, owing to the paucity of viable targets.
on the RGB that can be observed with DEIMOS. As a result, our routine has identified only 6 stars as potential members, highlighted in Figure 15. The dwarf has a systemic velocity of $v_r = -261.6^{+3.0}_{-2.8}$ km s$^{-1}$, and a fairly typical velocity dispersion of $\sigma_v = 8.6^{+2.8}_{-2.2}$ km s$^{-1}$. As with And XX, while we believe our routine can robustly measure the velocity dispersions of systems with only six confirmed members, to be truly confident of this value, follow up of And XXVI to increase the number of likely members is required.

In Conn et al. (2012), from an analysis of the photometry of And XXVI, they determined a distance modulus to the object of $(m-M)_0 = 24.39^{+0.55}_{-0.53}$ from a Markov Chain Monte Carlo analysis of the PAndAS photometry of And XXVI. This value corresponds to an $i$-band magnitude for the tip of the RGB (TRGB) of And XXVI of $m_{i,0} = 21.1^{+0.55}_{-0.53}$. Our CMDs for the dwarfs are not extinction corrected, but using the extinction values from Richardson et al. (2011) of $E(B-V) = 0.110$ (Schlegel et al. 1998), this would correspond to an $i$-band magnitude of $m_{i,TRGB} = 21.3^{+0.55}_{-0.53}$. Three targets were observed with magnitudes and colors that should be consistent with their belonging to And XXVI. However, we find that all these objects have velocities that are consistent with being Galactic foreground contaminants. Given the position of And XXVI in the northern M31 halo, where contamination from the MW increases, this is not unexpected. The brightest star we observe that is likely associated with And XXVI has $m_i = 21.9$.
Assuming that this brightest confirmed member star of And XXVI sits at the RGB tip, the distance estimate becomes 1.1 Mpc. While this value is higher than that of Conn et al. (2011), it is still within their upper distance estimate. Additionally, as not every star brighter than the member with $m_i = 21.7$ with colors consistent with the And XXVI RGB was observed, this value merely represents an upper limit, on the distance to And XXVI and highlights the difficulty of calculating distances to these faint galaxies where RGB stars are sparse.

4.11. Andromeda XXVII

Andromeda XXVII (And XXVII) is a somewhat unusual object as it is currently undergoing tidal disruption, spreading its constituent stars into a large stellar stream, named the northwestern arc, discovered in the PAndAS survey by Richardson et al. (2011). As such, it is unlikely to be in virial equilibrium, if it remains bound at all.

When determining the kinematics of And XXVII, we find the results to be somewhat unsatisfactory. Our routine determines $v_r = -539.6^{+4.5}_{-4.3}$ km s$^{-1}$ and $\sigma_v = 14.8^{+4.1}_{-3.1}$ km s$^{-1}$ from 11 stars. However, from an inspection of Figure 16, we see that there is significant substructure around $v_{hel} \sim -500$ km s$^{-1}$, much of which is considered to be unassociated with And XXVII in this analysis as it does not fall within a cold, well-defined Gaussian velocity peak. Given the disrupting nature of And XXVII, it is likely that a different analysis is...
required for this object, and we shall discuss this further in a future analysis, where the kinematics of the northwestern arc itself are also addressed. From this first pass, however, it would appear that And XXVII may no longer be a gravitationally bound system.

4.12. Andromeda XXVIII

And XXVIII was recently discovered in the eighth data release of the SDSS survey (Slater et al. 2011). It has $M_v = -8.5$ and $r_{\text{half}} = 210^{+50}_{-50}$ pc. It is also potentially one of Andromeda’s most distant satellites, with a host-satellite projected separation of $365^{+17}_{-1}$ kpc. The And XXVIII satellite is not covered by the PAndAS footprint, so we must instead use the original SDSS photometry for our analysis. A CMD with the SDSS $i$-band and $r - i$ colors for And XXVIII is shown in Figure 17, where all targets brighter that $i \sim 23.5$ within $3r_{\text{half}}$ are shown. The photometry here do not show an RGB that is as convincing as those from the PAndAS survey, so to guide the eye, we also overplot an isochrone from Dotter et al. (2008) with a metallicity of $[\text{Fe}/\text{H}] = -2.0$, corrected for the distance of And XXVIII as reported in Slater et al. (2011).

In a recent paper, Tollerud et al. (2013) discussed the kinematics of this object as derived from 18 members stars. They find $v_r = -328.0 \pm 2.3$ km s$^{-1}$ and $\sigma_v = 8.1 \pm 1.8$ km s$^{-1}$ from their full sample. They then remove two stars that they
We will use our derived parameters for this object in the remainder of our analysis.

4.13. And XXX/Cassiopeia II

And XXX—also known as Cass II owing to its spatial location, overlapping the Cassiopeia constellation—is a recently discovered dSph from the PAndAS survey (M. J. Irwin et al., in preparation). It has $M_v = -8.0$ and $r_{\text{half}} = 267^{+23}_{-36}$ pc. Located to the northwest of Andromeda, it sits within 60 kpc of the two close dwarf elliptical M31 companions, NGC 147.
and NGC 185. With these three objects found so close together in physical space, it is tempting to suppose them to be a bound system within their own right, but this can only be borne out by comparing their kinematics.

Conspiring to confound us, we find that Cass II has kinematics that place it well within the regime of Galactic foreground, as can be seen in Figure 18. However, our analysis is able to detect the dSph as a cold spike consisting of eight likely members. As for And XIX, we check the strength of the Na\textsc{i} doublet in these likely members, and find no significant absorption, making them unlikely foreground contaminants. We measure $v_r = -139.8^{+6.0}_{-6.0}$ km s$^{-1}$, and a fairly typical velocity dispersion of $\sigma_v = 11.8^{+7.7}_{-4.7}$ km s$^{-1}$.

The systemic velocity of Cass II ($v_r = -139.8^{+6.0}_{-6.0}$ km s$^{-1}$) puts it within $\sim 50$ km s$^{-1}$ of those of NGC 147 and NGC 185 ($v_r = -193 \pm 3$ km s$^{-1}$ and $v_r = -210 \pm 7$ km s$^{-1}$; Mateo 1998), lending further credence to the notion that these three systems are associated with one another. This will be discussed in more detail in M. J. Irwin et al. (2013, in preparation).

4.14. A Note on Previous Work

Finally, we also use our new algorithm to reanalyze all our previously published M31 dSph data sets. These include And V, VI (Collins et al. 2011), XI, XII, and XIII (Chapman et al. 2007; Collins et al. 2010). Details of the results of this reanalysis can
In previous studies by our group (Chapman et al. 2005; Letarte et al. 2009; Collins et al. 2010), we also published kinematic analyses for three additional M31 dSphs; And IX, And XV, and And XVI. In T12, it was noted that the values presented in these works for systemic velocities and velocity dispersions were not consistent with those measured in their analyses. We revisited these data sets in light of this discrepancy, to see if our new technique could resolve this issue. We found that these discrepancies remained. For And IX, we measure systemic velocity of $v_r = -204.8 \pm 2.1$ km s$^{-1}$, cf. $v_r = -209.4 \pm 2.5$ km s$^{-1}$ in T12 and a velocity dispersion of $\sigma_v = 2.0^{+0.7}_{-0.2}$ km s$^{-1}$, cf. $\sigma_v = 10.9 \pm 2.0$ km s$^{-1}$. Not only are their measurements determined from four times the member stars that we possess, we also experienced problems with our radial velocity measurements for the stars observed with this mask, due to the use of the minislitlet approach pioneered by...
the mass contained within the half-light radius ($M_{\text{1/2}}$), but recent work by Walker et al. (2009a) has shown that dark matter dominated they are. There are several methods in the measure masses for these systems, allowing us to infer how systems, we can use their internal velocity dispersions to measure $\sigma_v$ from $T_{12}$. We also note offsets in our velocity dispersions for many of the science spectra, lowering the quality of our radial velocity anisotropy of the tracer population; however, it is sensitive to the embeddedness of the stellar component within the DM halo. Particularly, the mass tends to be slightly overestimated the more embedded the stars are (Walker & PFINNAR 2011), especially if the dark matter halo follows a cored density profile.

As numerous authors have shown that the velocity dispersion profiles of dSphs are constant with radius (e.g., Walker et al. 2007, 2009b), we assume that our measured values of $\sigma_v$ are representative of the luminosity-averaged velocity dispersion ($\sigma_v$, half) used by Walker et al. (2009b). However, if it transpired that the velocity dispersion profiles of the Andromede dSphs were not flat, but declined or increased with radius, this would no longer true. We see no evidence for this behavior in our data set, although low-number statistics means we are unable to completely rule out this possibility. We calculate this for all our observed dSphs (including those we reanalyzed from previous works, see Appendix B) using results from the Keck LRIS and DEIMOS data set, and report their masses within $r_{\text{half}}$ ($M_{\text{half}}$) in Table 4.

From these masses, it is trivial to estimate the dynamical central mass-to-light ratios for the objects, $[M/L]_{\text{half}}$. We list these values for each dSph in Table 4, where the associated uncertainties also take into account those from the measured luminosities and distances to these dSphs (McConnachie 2012; Conn et al. 2012), as well as those on the masses measured in this work.

5. THE MASSES AND DARK MATTER CONTENT OF M31 dSphs

5.1. Measuring the Masses and Mass-to-light Ratios of Our Sample

As dSph galaxies are predominantly dispersion supported systems, we can use their internal velocity dispersions to measure masses for these systems, allowing us to infer how dark matter dominated they are. There are several methods in the literature for this (e.g., Illingworth 1976; Richstone & Tremaine 1986), but recent work by Walker et al. (2009a) has shown that the mass contained within the half-light radius ($M_{\text{half}}$) of these objects can be reliably estimated using the following formula:

$$M_{\text{half}} = \mu r_{\text{half}} \sigma_v^{2}$$  \hspace{1cm} (12)$$

where $\mu = 580$ $M_{\odot}$ pc$^{-1}$ km$^{-2}$ s$^{-2}$, $r_{\text{half}}$ is the spherical half-light radius in pc and $\sigma_v$ is the luminosity-averaged velocity dispersion. This mass estimator is independent of the (unknown) velocity anisotropy of the tracer population; however, it is sensitive to the embeddedness of the stellar component within the DM halo. Particularly, the mass tends to be slightly overestimated the more embedded the stars are (Walker & PFINNAR 2011), especially if the dark matter halo follows a cored density profile.

As numerous authors have shown that the velocity dispersion profiles of dSphs are constant with radius (e.g., Walker et al. 2007, 2009b), we assume that our measured values of $\sigma_v$ are representative of the luminosity-averaged velocity dispersion ($\sigma_v$, half) used by Walker et al. (2009b). However, if it transpired that the velocity dispersion profiles of the Andromede dSphs were not flat, but declined or increased with radius, this would no longer true. We see no evidence for this behavior in our data set, although low-number statistics means we are unable to completely rule out this possibility. We calculate this for all our observed dSphs (including those we reanalyzed from previous works, see Appendix B) using results from the Keck LRIS and DEIMOS data set, and report their masses within $r_{\text{half}}$ ($M_{\text{half}}$) in Table 4.

From these masses, it is trivial to estimate the dynamical central mass-to-light ratios for the objects, $[M/L]_{\text{half}}$. We list these values for each dSph in Table 4, where the associated uncertainties also take into account those from the measured luminosities and distances to these dSphs (McConnachie 2012; Conn et al. 2012), as well as those on the masses measured in this work.

5.2. Comparing the Mass-to-light Ratios of M31 and Milky Way dSphs

By combining our measurements of the kinematic of M31 dSphs in this work with those from T12 and Tollerud et al. (2013), we find ourselves with a set of kinematic properties as measured for 27 of the 28 Andromeda dSphs (owing to the difficulties experienced with the And XXIV data set, we do not include this object in our subsequent analysis). This nearly complete sample allows us to fully compare the masses
and mass-to-light ratios for the M31 satellite system with those measured in the MW satellites. Before beginning this analysis, we compile Table 5 which presents the kinematics for the full M31 satellite system, which combines the results from this work, T12, Kalirai et al. (2010), and Tollerud et al. (2013). In cases where two measurements for a dSph exist, we use those that were calculated from larger numbers of likely members, as these are the more robust. We begin by comparing the mass-to-light ratios (which indicate the relative dark matter dominance of these objects) of the two populations as a function of luminosity. In Figure 19 we show these values for all MW (red triangles, with values taken from Walker et al. 2009b), and M31 (blue circles) dSphs as a function of their luminosity. We can see that all these objects are clearly dark matter dominated, excluding And XII and And XVII where we are unable to resolve the mass with current data sets. We also see that they follow the trend of increasing $M/L_{\text{half}}$ with decreasing luminosity, as is seen in their MW counterparts.

The one tentative exception to this is the And XXV dSph. From our data set, we measure a value of $M/L_{\text{half}} = 10.3^{+7.0}_{-6.7}$ for this object, making it consistent with a stellar population with no dark matter within its 1σ uncertainties. This result is surprising and would be of enormous importance if confirmed with a larger data set than our catalog of 26 likely members as it would be the first dSph to be observed with a negligible dark matter component. And XXV is also one of the members of the recently discovered thin plane of satellites in Andromeda (Ibata et al. 2013), and so the presence or absence of dark matter in And XXV might tell us more about the origins of this plane, which are currently poorly understood.

5.3. Comparing the Masses of M31 and Milky Way dSphs

Finally, we discuss how the masses for the full sample of Andromeda dSphs for which kinematic data are available compare with those of the MW dSphs. For the M31 dSph population, we again use our compilation of kinematic properties assembled in Table 5. We plot the velocity dispersions, mass within the half-light radius, and central densities for all M31 (blue circles) and MW (red triangles; Walker et al. 2009b;
Adén et al. 2009; Koposov et al. 2011; Simon et al. 2011) dSphs as a function of radius in Figure 20. We then overplot the best-fit Navarro–Frenk–White (NFW) and cored mass profiles for the MW, taken from Walker et al. (2009b). In general, we see that the M31 and MW objects are similarly consistent with these profiles, an agreement that was also noted by T12. However, there are three objects which are clear outliers to these relations. These are And XIX, XXI, and XXV, with velocity dispersions of $\sigma_v = 4.7^{+1.6}_{-1.5}$ km s$^{-1}$, $\sigma_v = 4.5^{+1.2}_{-1.0}$ km s$^{-1}$, and $\sigma_v = 3.0^{+1.5}_{-1.2}$ km s$^{-1}$, as derived in this work. Given their half-light radii ($r_{\text{half}} = 1481^{+52}_{-50}$ pc, $r_{\text{half}} = 842 \pm 77$ pc, and $r_{\text{half}} = 642^{+47}_{-74}$ pc), one would expect them to have dispersions of closer to 9 km s$^{-1}$ in order to be consistent with the MW mass profile. As they stand, these three objects are outliers at a statistical significance of 2.5$\sigma$, 3.0$\sigma$, and 3.4$\sigma$ (calculated directly from their likelihood distributions as presented in Figures 8, 10, and 14). Similarly, in T12 they noted that And XXII and And XIV were outliers in the same respect as And XIX, XXI, and XXV, albeit at a lower significance. These differences can also be observed in terms of the enclosed masses and densities within $r_{\text{half}}$.

In Collins et al. (2011) we argued that the low velocity dispersion seen in some Andromeda dwarfs were a result of tidal forces exerted on their halos by the host over the course of their evolution, and that this effect was predominantly seen in dSphs where their half-light radii were more extended for a given luminosity than expected, such is the case our three outliers, And XIX, XXI, and XXV. This result therefore adds weight to the trend presented in that work. A number of recent works trying to account for the lower than predicted central masses of dSph galaxies within the Local Group also support this notion. For example, Peña­rrubia et al. (2010) demonstrated that the presence of a massive stellar disk in the host galaxy (such as those of the MW and M31) can significantly reduce the total masses of its associated satellites. In addition, recent papers by Zolotov et al. (2012) and Brooks & Zolotov (2012), where the effect of baryons within dark matter only simulations was measured also find that tidal forces exerted by host galaxies where a massive disk is present will serve to reduce the masses of its satellite population at a far greater rate than hosts without baryons. And XIX, XXI, and XXV may thus represent a population of dSph satellites whose orbital histories about M31 have resulted in substantial fractions of their central mass being removed by tides. It should be noted, however, that tides not only reduce the central masses and densities of dSph halos, they also reduce the spatial size of the luminous component (Peña­rrubia et al. 2008b, 2010), albeit at a slower rate. The tidal scenario is therefore slightly difficult to reconcile with these outlying M31 dSphs having the largest sizes, unless they were both more massive and spatially larger in the past.

Other recent theoretical works have also shown that the removal of baryons from the very centers of dark matter halos by baryonic feedback (from star formation and supernovae, for example) can also help to lower the central masses and densities of satellite galaxies (e.g., Pontzen & Governato 2012; Zolotov et al. 2012; Brooks & Zolotov 2012). For this method to work effectively, however, very large “blow outs” of gas are required, of the order $\sim 10^8$–$10^9 M_\odot$, equivalent to $\sim 40,000$ supernovae. This would require a minimum initial satellite luminosity of $M_V < -12$ (Zolotov et al. 2012; Garrison-Kimmel et al. 2013), significantly brighter than the current luminosities of our outliers ($M_V \sim -10$). Therefore, if feedback has indeed played a role in the shaping of the dark matter halos of And XIX, XXI, and XXV, one assumes it would have to have operated in tandem with tidal stripping. We will discuss the implications and interpretation of these result further in a companion paper (M. L. M. Collins et al., in preparation).
Figure 21. Figures of the S/N weighted composite spectra for each dSph. The average metallicity for each dSph, plus the associated uncertainty is printed on each panel (continued over page).

(A color version of this figure is available in the online journal.)
Figure 22. Figures of the S/N weighted composite spectra for each dSph (excluding And XV and And XVI). The average metallicity for each dSph, plus the associated uncertainty is printed on each panel (continued over page).

(A color version of this figure is available in the online journal.)

6. METALLICITIES

Our observational setup was such that we cover the calcium triplet region (Ca\textsc{ii}) of all our observed stars. This strong absorption feature is useful not only for calculating velocities for each star, but also metallicities. For RGB stars, such as we have observed, there is a well known relation between the EWs of the Ca\textsc{ii} lines, and the iron abundance, [Fe/H], of the object. The calibration between these two values has been studied and tested by numerous authors, using both globular clusters and dSphs, and is valid down to metallicities as low as [Fe/H] $\sim -4$ (see, e.g., Battaglia et al. 2008; Starkenburg et al. 2010). Following the Starkenburg et al. (2010) method, which extends the sensitivity of this method down to as low as [Fe/H] $\sim -4$, we fit Gaussian functions to the three Ca\textsc{ii} peaks to estimate their EWs, and calculate [Fe/H] using Equation (13):

\[
[\text{Fe/H}] = -2.87 + 0.195(V_{\text{RGB}} - V_{\text{HB}}) + 0.48\Sigma\text{Ca} - 0.913\Sigma\text{Ca}^{-1.5} + 0.0155\Sigma\text{Ca}(V_{\text{RGB}} - V_{\text{HB}}),
\]

(13)

where $\Sigma\text{Ca} = 0.5(\text{EW}_{8498} + \text{EW}_{8542} + 0.6\text{EW}_{8662})$. $V_{\text{RGB}}$ is the magnitude (or, if using a composite spectrum, the average,
more robust determination of the average metallicities we co-
add the spectra for each dSph (weighting by the S/N of each
individual stellar spectrum, which is required to be a minimum
of 2.5 Å⁻¹) and measure the resulting EWs. In a few cases, not
all three Ca ii lines are well resolved. For And V, IX, XVII,
XVIII XXVI, and XXVIII, the third Ca ii line is significantly
affected by skylines, while for And XXIV, the first Ca ii line
is distorted. In the case of And XIII, only the second Ca ii line
appears well resolved. In these cases, we neglect the affected
lines in our estimate of [Fe/H], and derive reduced EWs from
the unaffected lines. Where the third line is affected, this gives
ΣCa = 1.5EW8498+EW8542. Where the second line is affected,
we find ΣCa = EW8542+EW8662. Finally, where only the second
line seems reliable we use ΣCa = 1.7EW8542. These coefficients
are derived empirically from high S/N spectra where the absolute
values of [Fe/H] are well known. We test these variations of ΣCa
by applying them to our high S/N co-added spectra where all three lines are well resolved, such as And XXI and XXV, and we find that all three formulae produce consistent values of [Fe/H]. The composite spectra for each satellite are shown in Figures 21 and 22. In all cases, we find that our results are consistent with photometric metallicities derived in previous works.

In the MW, it has been observed that the average metallicities of the dSph population decrease with decreasing luminosity (e.g., Kirby et al. 2008, 2011). In Figure 23, we plot the spectroscopic metallicities of the M31 dSphs (blue dSphs) as a function of absolute magnitude. We plot the MW dSphs as red triangles (Martin et al. 2007; Kirby et al. 2008, 2011; Belokurov et al. 2009; Koch et al. 2009). We also include those M31 dSphs for which only photometric measurements of [Fe/H] are available (And I, II, III, VII, and XIV; Kalirai et al. 2010; T12), and these are highlighted as encircled blue points. The dashed line represents the best-fit to the MW dSph population from Kirby et al. (2011). The three relatively metal rich ([Fe/H] ~ −1.5 to −2.0), faint (L ~ 1000 L_☉) MW points are the three ultra-faint dSphs Willman I, Boötes II, and Segue 2, and these three were not included in the Kirby et al. (2011) analysis, where the best fit MW relation was determined. We see that the metallicities for a given luminosity in the M31 dSphs also loosely define a relationship of decreasing metallicity with decreasing luminosity, and they agree with that defined by their MW counterparts within their associated uncertainties. However, it is also noteworthy that for dSphs

16 This assumed value is sensitive to age and metallicity effects, see Chen et al. 2009 for a discussion, however owing to the large distance of M31, small differences in this value within the M31 system will have a negligible effect on metallicity calculations.

Figure 23. Spectroscopically derived [Fe/H] vs. luminosity for all MW (red triangles, taken from Kirby et al. 2011, with additional measurements taken from Martin et al. 2007; Belokurov et al. 2009; Koch et al. 2009) and M31 dSphs (blue circles, this work). The solid line represents the best fit relationship between these two parameters as taken from Kirby et al. (2011). The dashed lines represent the 1σ scatter about this relationship. We see that the M31 dSphs follow this relationship very well within their associated uncertainties. As we discuss in Section 6, those galaxies with L < 10^6 L_☉ are also consistent with having a constant metallicity, which could indicate a metallicity floor in these fainter systems.

(A color version of this figure is available in the online journal.)

with L < 10^6 L_☉, the Andromeda satellites are also consistent with having a constant metallicity of ~−1.8. The same leveling off of average metallicity at lower luminosities was noted by McConnachie (2012), where they note that this break occurs at the same luminosity as a break in the luminosity-surface brightness relation for faint galaxies. As such, it could imply that the density of baryons in these systems, rather than the total number of baryons, could be the most important factor in determining their chemical evolution. The error bars we present here are still significant, so it is hard to fully interpret this result, but the hint of a metallicity floor in these lower luminosity systems is intriguing.

In Figure 23, we highlight the positions of our three kinematic outliers, And XIX, XXI, and XXV, and we see that they fall almost exactly on the MW relation. In this figure, systems that have experienced extreme tidal stripping would move horizontally to the left, as their luminosity would gradually decrease as stars are stripped, but their chemistry would remain unaffected. One would expect to see such behavior only after the stellar component began to be removed in earnest, after the majority of the dark matter halo had been removed. If their central densities were lowered by some active feedback mechanism, such as SN II explosions (e.g., Zolotov et al. 2012), one would expect the objects to become more enriched and perhaps brighter, moving them up and to the right, potentially allowing them to remain on the MW relation. To confirm that this was the case for And XIX, XXI, and XXV, we would require more information on the abundances of these objects and their star formation histories, which we do not currently possess.
7. CONCLUSIONS

Using new and existing spectroscopic data from the Keck I/LRIS and Keck II/DEIMOS spectrographs, we have homogeneously derived kinematic properties for 18 of the 28 known Andromeda dSph galaxies. Using a combination of their $g - i$ colors, positions on the sky and radial velocities, we determine the likelihood of each observed star belonging to a given dSph, thus filtering out MW foreground or M31 halo contaminants. We have measured both their systemic velocities and their velocity dispersions, with the latter allowing us to constrain the mass and densities within their half-light radii. For the first time, we confirm that And XVII, XIX, XX, XXIII, XXVI, and Cass II are dark matter dominated objects, with dynamical mass-to-light ratios within the half-light radius of $[M/L]_{\text{half}} > 10 M_\odot/L_\odot$.

For And XXV, a bright M31 dSph ($M_V = -9.7$) we measure a mass-to-light ratio of only $[M/L]_{\text{half}} = 10.3^{+7.0}_{-6.7} M_\odot/L_\odot$ from a sample of 26 stars, meaning that it is consistent with a simple stellar system with no appreciable dark matter component within its 1σ uncertainties. If this were confirmed with larger data sets, it would prove to be a very important object for our understanding of the formation and evolution of galaxies.

We compare our computed velocity dispersions and mass estimates with those measured for MW dSphs, and find that the majority of the M31 dSphs have very similar mass–size scalings to those of the MW. However, we note three significant outliers to these scalings, namely And XIX, XXI, and XXV, which possess significantly lower velocity dispersions than expected for their size. These results build on the identification of three potential outliers in the T12 data set (And XIV, XV, and XVI). We suggest that the lower densities of the dark matter halos for these outliers could be an indication that they have encountered greater tidal stresses from their host over the course of their evolution, decreasing their masses. However, these bright systems still fall on the luminosity–metallcity relationship established for the dSph galaxies of the Local Group. If these objects have undergone significant tidal disruption, we would expect them to lie above this relation. As such, this remains puzzling, and requires dedicated follow up studies to fully map out the kinematics of these unusual systems.

We measure the metallicities of all 18 dSphs from their co-added spectra and find that they are consistent with the established MW trend of decreasing metallicity with decreasing luminosity.

This work represents a significant step forward in understanding the mass profiles of dwarf spheroidal galaxies. Far from residing in dark matter halos with identical mass profiles, we show that the halos of these objects are complex, and differ from one to the next, with their environment and tidal evolution imprinting themselves upon the dynamics of their stellar populations. The Andromeda system of dSphs presents us with an opportunity to better understand these processes, and our future work will further illuminate the evolutionary paths taken by these smallest of galaxies.

We would like to thank Hans-Walter Rix for helpful discussions regarding this manuscript. We are also grateful to the referee for their helpful and detailed suggestions for improving this work. We thank the SPLASH collaboration for providing us with details of their observations of dSphs as presented in T12.

Most of the data presented herein were obtained at the W. M. Keck Observatory, which is operated as a scientific partnership among the California Institute of Technology, the University of California and the National Aeronautics and Space Administration. The Observatory was made possible by the generous financial support of the W. M. Keck Foundation.

Based in part on observations obtained with MegaPrime/MegaCam, a joint project of CFHT and CEA/DAPNIA, at the CFHT which is operated by the National Research Council (NRC) of Canada, the Institute National des Sciences de l’Univers of the Centre National de la Recherche Scientifique of France, and the University of Hawaii.

Based in part on data collected at Subaru Telescope, which is operated by the National Astronomical Observatory of Japan.

The authors wish to recognize and acknowledge the very significant cultural role and reverence that the summit of Mauna Kea has always had within the indigenous Hawaiian community. We are most fortunate to have the opportunity to conduct observations from this mountain. Funding for SDSS-III has been provided by the Alfred P. Sloan Foundation, the Participating Institutions, the National Science Foundation, and the U.S. Department of Energy Office of Science. The SDSS-III Web site is http://www.sdss3.org/.

SDSS-III is managed by the Astrophysical Research Consortium for the Participating Institutions of the SDSS-III Collaboration including the University of Arizona, the Brazilian Participation Group, Brookhaven National Laboratory, University of Cambridge, Carnegie Mellon University, University of Florida, the French Participation Group, the German Participation Group, Harvard University, the Instituto de Astrofisica de Canarias, the Michigan State/Notre Dame/JINA Participation Group, Johns Hopkins University, Lawrence Berkeley National Laboratory, Max Planck Institute for Astrophysics, Max Planck Institute for Extraterrestrial Physics, New Mexico State University, New York University, Ohio State University, Pennsylvania State University, University of Portsmouth, Princeton University, the Spanish Participation Group, University of Tokyo, University of Utah, Vanderbilt University, University of Virginia, University of Washington, and Yale University.

R.I. gratefully acknowledges support from the Agence Nationale de la Recherche though the grant POMMME (ANR 09-BlAN-0228).

G.F.L. gratefully acknowledges financial support for his ARC Future Fellowship (FT100100268) and through the award of an ARC Discovery Project (DP110100678).

N.B. gratefully acknowledges financial support through the award of an ARC Discovery Project (DP110100678).

A.K. thanks the Deutsche Forschungsgemeinschaft for funding from Emmy-Noether grant Ko 4161/1.

APPENDIX A

TESTING THE MEMBERSHIP PROBABILITY ALGORITHM

A.1. The Inclusion of a Velocity Term in the Calculation of $P_i$

In T12, the authors do not impose a velocity probability criterion for their membership calculations. Instead they require all member stars to have a total probability, based on their positions and colors, of $P_{\text{member}} > 0.1$, and then apply a 3σ clipping to this final sample to prevent any outliers from significantly inflating their calculated velocity dispersions. In our analysis, we have avoided making any hard cuts to our sample by also utilizing prior information on the velocities of our expected contaminant populations and member stars. In Section 3.3, we tested that our velocity probability criteria was not overly biasing our final measurements of velocity dispersion
to artificially lower values with the introduction of an extra parameter, $\eta$, that allows us to add additional weight to stars in the tails of the Gaussian velocity distribution. However, we can further test our velocity criterion by removing it entirely from the probabilistic determination, and instead implementing the same cuts presented by T12. This involves cutting stars where $P_i < 0.1$ (as determined from $P_{\text{CMD}}$ and $P_{\text{data}}$), and also by iteratively removing all stars that have velocities that do not lie within $3\sigma$ of the mean of the remaining sample. In Table 6, we present the results of this on our measured values of $v_r$ and $\sigma_v$ for our full sample of dSphs. For all objects (barring And XXVII, which is a unique case, as described in Section 4.11) the systemic velocities derived are within $\sim2\pm3$ km s$^{-1}$ of one another. The velocity dispersions we measure from our full algorithm tend to be slightly higher on average, and this is to be expected as we do not cut any stars from our analysis, and therefore outliers in the velocity profile may be assigned non-negligible membership probabilities that will allow them to increase this measurement. By and large, these differences are not significant, with the final values agreeing to well within their $1\sigma$ uncertainties.

It is interesting that our algorithm appears to perform better when dealing with dSphs where the number of member stars is low. This is best demonstrated by And XI (see Figure 24). Our algorithm identifies five stars with non-negligible probabilities of membership, clustered around $v_r \sim -430$ km s$^{-1}$. Our full algorithm measures a systemic velocity of $v_r = -427.5 \pm 3.3$ km s$^{-1}$ and a velocity dispersion of $\sigma_v = 7.5^{+3.3}_{-2.8}$ km s$^{-1}$. One of these stars is slightly offset from the other four with a more negative velocity of $v_r = -456.8$ km s$^{-1}$. Although this star has a reasonably high probability of being a member based on its distance from the center of And XI, and its position in the CMD, it does not survive the $3\sigma$ velocity clipping procedure of T12. As the number of member stars is so low, cutting one star from the sample can have a significant effect, and as such, while the T12 procedure determines a very similar systemic velocity of $v_r = -425.0 \pm 3.1$ km s$^{-1}$ it is unable to resolve a velocity dispersion. This effect is also seen other systems (such as And XIII, XVII, XXII, and XXVI), although it is typically less pronounced.

Another regime where our algorithm performs better than that of T12 is where the systemic velocity of the system in question is within the regime of the contaminating MW K-dwarfs. An example of this is the unusual system, And XIX, where our algorithm measures a systemic velocity of $v_r = -111.6^{+1.6}_{-1.4}$ km s$^{-1}$ and a velocity dispersion of $\sigma_v = 4.7^{+1.6}_{-1.4}$. However, the procedure of T12 is less able to resolve the kinematics of the system, measuring $v_r = -109.3 \pm 5.3$ km s$^{-1}$ and a velocity dispersion of $\sigma_v = 1.8^{+9.1}_{-1.8}$. The much larger uncertainty on the dispersion is a result of including MW contaminants in the sample which can be difficult to cut out without applying prior knowledge of the velocity profile of this population. $3\sigma$ clipping allows outliers to contribute more significantly to the measured profile in this instance, increasing the uncertainty. A similar effect is seen in the And XXIV and And XXX (Cass II) objects, which also have systemic velocities in the MW contamination regime.

These results lead us to conclude that the inclusion of a $P_{\text{vel}}$ term in our analysis allows us to more effectively determine the true kinematics of the systems we are studying. Further, as no cuts to the sample are required using this method, it allows for a more unbiased study of the kinematics of dSphs than that of T12.

### A.2. The Effect of Low Signal-to-noise Data on Measuring $v_r$ and $\sigma_v$

For our brightest targets ($i < 22.5$) the S/N of our spectra is typically $>3$ Å$^{-1}$. However, as our targets become fainter, so too their S/N falls. For spectra with S/N $\gtrsim 1.5$ Å$^{-1}$, our pipeline is still able to measure velocities based on the CaII triplet, with reasonable measurement uncertainties. However, it is prudent to check whether the inclusion of these velocities, calculated from significantly noisier spectra, has a detrimental effect on our ability to measure the kinematic properties of our dSph sample.

Such a test is straightforward to implement. We have a number of dSphs within our sample for which our probabilistic analysis identifies $\sim30$ likely members (such as And XXI, XXIII, and XXV). We can therefore use these samples to impose S/N cuts on our data to see the effect of this on our measurements of $v_r$ and $\sigma_v$. We present the results of this test in Table 7, and our finding is that, as the level of our imposed S/N cut increases (and so the number of included stars decreases), the systemic velocity remains more or less constant. The measured velocity dispersion, however, shows some variation. In the case of And XXI and XXV, the dispersion increases with increased S/N, however not significantly. In both cases the dispersion calculated from the higher S/N data lies well within $1\sigma$ of that calculated from the lower S/N data. Intuitively, this makes sense as the spectra with higher S/N are likely to have lower velocity uncertainties, and so our maximum-likelihood analysis will attribute more of the spread in measured velocities to an intrinsic dispersion, rather than to our measurement errors. In the case of And XXIII, we find the opposite to be true. As our S/N cut increases, we find that our measured dispersion decreases. This may be because the number of member stars in subsequent quality cuts drops off more rapidly for And XXIII than And XXI and XXV. This suggests that we should be extra...
Figure 24. As Figure 6, but for And XI. Using our full probabilistic algorithm (including our $P_{\text{vel}}$ term), five stars are identified as likely members. When implementing the 3σ clipping of T12, the star with $v_r \sim -450$ km s$^{-1}$ is removed from the analysis, despite having a high probability of membership based on its color ($P_{\text{CMD}}$) and distance from the center of the dSph ($P_{\text{dist}}$). This has a substantial effect on the calculated velocity dispersion, as shown in Table 6.

(A color version of this figure is available in the online journal.)

Table 7

The Effect of Including Low S/N Data in Our Analysis on Determining $v_r$ and $\sigma_v$

| Object  | And XXI | And XXII | And XXIII | And XXV |
|---------|---------|----------|-----------|---------|
| $N_x$   | $v_r$ (km s$^{-1}$) | $\sigma_v$ (km s$^{-1}$) | $v_r$ (km s$^{-1}$) | $\sigma_v$ (km s$^{-1}$) |
| $S/N > 2$ | 20 | $-362.9 \pm 0.9$ | $3.5^{+0.9}_{-0.7}$ | $-238.0 \pm 1.2$ | $6.6 \pm 1.1$ | 27 | $-107.7 \pm 0.9$ | $2.7 \pm 1.1$ |
| $S/N > 3$ | 11 | $-364.2 \pm 0.9$ | $3.1 \pm 0.8$ | $-238.5 \pm 1.4$ | $5.1^{+1.4}_{-1.2}$ | 24 | $-107.7 \pm 1.0$ | $3.0 \pm 1.2$ |
| $S/N > 4$ | 5 | $-363.9 \pm 1.5$ | $4.0^{+1.5}_{-1.1}$ | $-239.4 \pm 1.1$ | $5.7^{+1.5}_{-1.3}$ | 16 | $-108.2 \pm 1.2$ | $3.0^{+1.4}_{-1.2}$ |
| $S/N > 5$ | 3 | $-362.6^{+2.2}_{-2.3}$ | $4.5^{+2.6}_{-1.5}$ | $-239.5 \pm 1.9$ | $0.0^{+4.9}_{-1.3}$ | 13 | $-109.0 \pm 1.2$ | $2.8^{+1.5}_{-1.3}$ |
cautious when interpreting our measured velocity dispersions for dSphs where both the average S/N of member stars, and the number of member stars, is low.

A.3. The Effect of Small Sample Sizes on Determining Kinematic Properties of Dwarf Galaxies

Obtaining reliable velocities for member stars of faint and distant systems is a difficult task that can only be achieved with the largest optical telescopes, such as Keck. Given the demand for facilities such as this, any observing time awarded must be used as effectively as possible, and this often means compromising between deep pointings for a few objects, and shallower pointings for a number of objects. With longer or multiple exposures on a single target, one can build up impressive samples of member stars for an individual dSph. For example, the SPLASH collaboration observed a total of 95 members in And II, one of the brightest M31 dSph companions (Ho et al. 2012) by taking two separate exposure fields over this large object. However, multiple exposures such as these produce diminishing returns as you move down the luminosity scale to fainter, more compact dSphs. This is both because of their smaller size with respect to the DEIMOS field of view, and the fewer number of bright stars available on the RGB to target. In this case, the only way to identify more members is by integrating for longer, but given the paucity of stars, the trade-off between time spent exposing and additional members observed can be quite expensive. Such difficulties inevitably lead to the inference of dynamical properties for an entire system from a handful of stars. It is important for us to understand the effect this bias has on our results, and how reliable the quoted values are. We test this using our data sets for which we identify >25 member stars, namely And XIX, XXI, XXII, and XXV using the following method. We select 4, 6, 8, 10, 15, 20, 25, and 30 stars at random from each data set and then measure the systemic velocity and velocity dispersion using our probability algorithm. This was repeated 1000 times for each sample size. In cases where we are unable to resolve a dispersion, we find that our resulting uncertainties are not meaningful. This is shown explicitly in the case of And XVIII, where we can compare our upper limit for the velocity dispersion as determined from our algorithm with the dispersion calculated in T12 from a much larger data set. We see that our uncertainty is not consistent with their result. As such, we advise that in all cases where we calculate velocity dispersions from small samples ($N_\ast < 8$, And XI, XII, XXXIV, and XXVI), the dispersion measurements should be treated as indications of the likely dispersion, and need to be confirmed with follow-up studies.

A.4. Testing Our Algorithm on the SPLASH Sample of M31 dSphs

In T12, the authors reported on the kinematic properties of 15 M31 dSphs, And I, II, III, V, VII, IX, X, XI, XII, XIII, XIV, XV, XVI, XVIII, XX, and XXII, and the positions, and measured velocities (plus uncertainties) for each likely member stars were published as part of that work. The authors were kind enough to also give us access to these properties for their non-member stars so that we might run our algorithm over the full samples to see if we reproduce their results. Our technique for assigning membership probability differs from theirs in that we use the velocities of stars as an additional criterion for membership, whereas they use a cut on both the resulting probability ($P_{\text{member}} > 0.1$), and a 3$\sigma$ clipping on the velocity. In addition, where we use PAndAS CFHT/MegaCam g- and i-band photometry for our membership analysis, the SPLASH team use their own Washington-DDOS1 filter photometric data set, in membership classification. As such, small differences might be expected, but if our technique is robust our results should well mirror those of T12. In Table 9 we compare our calculated values of $v_r$ and $\sigma_v$ to those published in T12. As the measurements made in T12 for And XI and XII are made from only two stars, we do not include these in this test. In general, the results from both analyses agree to within 1$\sigma$ of one another, with the majority of them being well within this bound. Typically, we find that our procedure measures slightly larger values for $\sigma_v$ than that of T12 (with the exception of And IX, And XVII, and And XXII). This is to be expected, as we do not cut stars from our analysis based on their velocity, instead we down-weight their probability of membership. As such, those stars considered as outliers would naturally inflate simulations even when dealing with sample sizes as small as four stars, so long as the measurement is resolved. In cases where we are unable to resolve a dispersion, we find that our resulting uncertainties are not meaningful. This is shown explicitly in the case of And XVIII, where we can compare our upper limit for the velocity dispersion as determined from our algorithm with the dispersion calculated in T12 from a much larger data set. We see that our uncertainty is not consistent with their result. As such, we advise that in all cases where we calculate velocity dispersions from small samples ($N_\ast < 8$, And XI, XII, XXXIV, and XXVI), the dispersion measurements should be treated as indications of the likely dispersion, and need to be confirmed with follow-up studies.
our dispersions above those measured by T12, but the effect is marginal. These results demonstrate that our technique for assigning probability of membership of individual stars within M31 dSphs based on their photometric properties and velocities is robust, and comparable to that of T12. However, as discussed in Appendix A.1, we find that our technique is superior as it requires no cuts to the final data set to be made, reducing the bias in these measurements.

APPENDIX B
REANALYZING OUR PREVIOUSLY PUBLISHED RESULTS

To ensure our analysis of the global properties of the M31 dSph population in Section 5.1 is homogenous, we reanalyzed our previously published data sets using our new probability algorithm. Here we briefly summarize the results of this analysis and compare the new results to the published works. The objects we discuss here are And V, VI (first published in Collins et al. 2011), XI, XII, and XIII (published in Chapman et al. 2005, 2007; Collins et al. 2010). And V was observed with the LRIS instrument, while the remaining objects were observed with the DEIMOS instrument.

B.1. Andromeda V

Andromeda V (And V) was observed using the LRIS instrument on Keck I rather than the DEIMOS instrument on Keck II. LRIS has a lower resolution than DEIMOS, and a smaller field of view, which lowers the accuracy of velocity measurement and limits us to only ∼50 targets within a mask compared with 100–200 for a DEIMOS mask. The raw data were also not reduced using our standard pipeline, owing to problems with the arc-lamp calibrations, and were instead analyzed using the NOAO.ONESPEC and NOAO.TWODSPEC packages in IRAF. The results from this reduction, plus an analysis of the data using hard cuts in velocity, distance and color to determine membership were first published in Collins et al. (2011). Our full probabilistic analysis identifies 17 stars with a non-negligible probability of belonging to And V. Our technique determines a systemic velocity of $v_s = -391.5 \pm 2.7 \text{ km s}^{-1}$ and $\sigma_v = 12.5 \pm 0.5 \text{ km s}^{-1}$. Comparing these values to our previously published results ($v_s = -393.1 \pm 4.2 \text{ km s}^{-1}$ and $\sigma_v = 11.5 \pm 4.2 \text{ km s}^{-1}$; Collins et al. 2011) we find them to be consistent within the quoted uncertainties. We also compare our results to those of T12, who measured $v_s = 397.3 \pm 1.5 \text{ km s}^{-1}$ and $\sigma_v = 10.5 \pm 1.1 \text{ km s}^{-1}$ from a larger sample of stars (85 members, cf. 17) using the higher resolution DEIMOS spectrograph. The velocity dispersions of both are consistent within their 1σ uncertainties, as are the systemic velocities. Given the difference of a factor of five in number of probable member stars between our study and that of T12, this consistency is reassuring, and accurately determine the kinematics of M31 dSph galaxies from small sample sizes.

B.2. Andromeda VI

As And VI sits at a large projected distance from the center of M31 (∼270 kpc), it was not observed as part of the PAndAS survey and we were unable to use CFHT data for our $P_{\text{CMD}}$ determination. Instead, we use Subaru SuprimeCam data (PI: N. Arimoto, see Collins et al. 2011 for a full discussion of this data). Using our full probabilistic analysis, we identify 45 stars with $P > 10^{-6}$. Our technique determines a most likely $v_s = -339.8 \pm 1.8 \text{ km s}^{-1}$, with $\sigma_v = 12.4 \pm 1.5 \text{ km s}^{-1}$. Comparing these values with the results of Collins et al. (2011) who measured $v_s = -344.8 \pm 2.5 \text{ km s}^{-1}$ and $\sigma_v = 9.4 \pm 0.5 \text{ km s}^{-1}$, we see that both the systemic velocities and the velocity dispersions are consistent within quoted uncertainties. The slight differences between our previous study and this work are simply a result of the application of our new technique.

B.3. Andromeda XI

The kinematic properties for Andromeda XI as measured from this DEIMOS data set were first published in Collins et al. (2010). Here we identify five stars as probable members. We determine most likely parameters of $v_s = -427.5 \pm 3.4 \text{ km s}^{-1}$ and $\sigma_v = 7.6 \pm 1.0 \text{ km s}^{-1}$. In Collins et al. (2010) we measured $v_s = -419.4 \pm 4.5 \text{ km s}^{-1}$ and we were unable to resolve the velocity dispersion for the dSph, measuring $\sigma_v = 0.0 \pm 4.6 \text{ km s}^{-1}$ (where the upper bound represents the formal 1σ uncertainty on the unresolved dispersion), which implied a higher systemic velocity and lower velocity dispersion for And XI. However, in that analysis, one star with a velocity of $-440 \text{ km s}^{-1}$ was considered to be an outlier based on its velocity, and thus excluded from the kinematic analysis. Here, our algorithm gives this star a non-zero probability of membership, which likely decreases the systemic velocity and increases the dispersion. T12 also presented observations for And XI, but they were not able to cleanly detect the galaxy. They identified two stars with highly negative velocities ($\sim 460 \text{ km s}^{-1}$), which are offset from our systemic velocity by $\sim 30 \text{ km s}^{-1}$. Given the very negative velocities of their two stars, the probability of them both being M31 contaminants seems low, and some other explanation may be more suitable. Between observations, there is one star common to both ($\alpha = 00:46:19.10, \delta = +33:48:4.1$), for which we measure a velocity of $-427.16 \text{ km s}^{-1}$ compared with $-461.6 \text{ km s}^{-1}$. This amounts to a statistical difference at the level of 5σ. One obvious avenue to check is that there has been no velocity offset introduced by a rogue skyline that falls within the region of one of the three Ca ii lines. We have carefully checked the spectra of each of our five probable members to see if this has been the case. We also rederive the velocity based on cross-correlations with each of the three lines individually, rather than with the full triplet. We find these results, and their
average to be entirely consistent within the associated errors from the velocities derived using the technique discussed in Section 2.2. This large discrepancy is puzzling, particularly as the methods used to measure velocities in this work are almost identical to those of T12. Without further data it is not possible for either team to pin down the exact issue, or which of the data sets gives the true systemic velocity. This argues for taking further observations within these faint systems, in the hopes of better understanding both the systems themselves, and any systematics introduced by the DEIMOS instrument. It is comforting that, in all cases where this offset is observed, the velocity dispersions measured by each team are consistent with one another, suggesting the problem affects all observations identically.

In this case, we have identified a greater number of potential members stars than in the work of T12, the spectra for all of which have relatively high S/N (S/N ~ 5–10 A⁻¹). Therefore, our results should be considered as more robust than those of T12.

B.4. Andromeda XII

Kinematic properties for Andromeda XII as determined from the DEIMOS data set presented here were previously published in Chapman et al. (2007) and Collins et al. (2010), and in both cases, membership was largely determined using hard cuts in velocity. This object has been of particular interest as it possesses an extremely negative systemic velocity with respect to Andromeda, suggesting that it is on its first infall into the local group (see Chapman et al. 2007 for a full discussion). Using our new algorithm, we measure $v_r = -557.1$ km s⁻¹ and an unresolved velocity dispersion of $\sigma_v = 0.0^{+0.0}_{-0.0}$ km s⁻¹, where the upper bound represents the formal 1σ uncertainty on the measurement. As the dispersion is unresolved, the lower error bound is undefined, as having a negative velocity dispersion is unphysical. These values are completely consistent with the results of Chapman et al. (2007) and Collins et al. (2010) ($v_r \approx -558.4 \pm 3.2$ km s⁻¹ and $\sigma_v = 2.6^{+3.6}_{-2.6}$ km s⁻¹). T12 also presented observations for And XII, but as for And XI, they were not able to cleanly detect the galaxy. They identified two stars with highly negative velocities ($\sim -530$ km s⁻¹), which are offset from our systemic velocity by $\sim 30$ km s⁻¹. In this instance, both the stars they observed overlapped with two of our likely members, situated at $\alpha = 00:47:28.63$, $\delta = +34:22:43.1$ and $\alpha = 00:47:24.69$, $\delta = +34:22:23.9$, and these velocities are offset from those that we measure at a statistical level of 3.8σ. This suggests that the self-same calibration effect that causes an offset between our results for And XI and those of T12, is present here also. In the case of And XII, our mask was observed over two separate nights, giving us two velocity measurements for each star (as discussed in Chapman et al. 2007 and Collins et al. 2010), and we saw no evidence for systematic offsets of this magnitude in the night to night velocities, making a calibration error within our data set seem unlikely, though not impossible. We therefore conclude that, owing to our larger sample of members and repeat observations, our measurements for the kinematic properties of And XII are more robust than those of T12.

B.5. Andromeda XIII

The kinematic properties of Andromeda XIII were also presented in Collins et al. (2010), and XIII sits at a large projected distance from Andromeda ($\sim 120$ kpc) in the southern M31 halo, so we expect contamination from the MW and Andromeda halo to be low. It is surprising then, that we see significant structure within our DEIMOS field. This is also seen within the three fields observed by T12, who attribute this over-density of stars located at $v_r \sim -120$ km s⁻¹ to an association with the TriAnd over-density within the Galactic halo. We too see a number of stars between $-140$ km s⁻¹ and $-100$ km s⁻¹. From their positions within the CMD of And XIII, they appear more consistent with MW foreground K-dwarfs than M31 RGB stars. As such, these are also likely associated to this MW substructure.

Using our full probabilistic analysis, we identify the most probable And XIII stars as those four that cluster around $v_r \sim -200$ km s⁻¹, and we determine $v_r = -204.8 \pm 4.9$ km s⁻¹ and are unable to resolve a velocity dispersion, with $\sigma_v = 0.0^{+8.1}_{-0.0}$ km s⁻¹, where the upper limit indicates the formal 1σ uncertainty on the likelihood distribution. Given the very large uncertainties on these values (mostly a factor of the low number of member stars) it comes as no surprise perhaps that these results are consistent with the results in Collins et al. (2010) ($v_r = -195.0^{+0.5}_{-1.8}$ km s⁻¹ and $\sigma_v = 9.7^{+3.6}_{-4.5}$), although not with those of T12 ($v_r = -185.4 \pm 2.4$ km s⁻¹ and $\sigma_v = 5.6 \pm 2.0$ km s⁻¹), where they derived parameters from three times the number of member stars that we present here. Given the highly substructured nature of the And XIII field, and the fact that our detection is at a very low significance (only four stars), we find that the T12 measurements for the kinematics of And XIII are more robust than ours.

REFERENCES

Aaronson, M. 1983, ApJL, 266, L11
Adén, D., Wilkinson, M. I., Read, J. I., et al. 2009, ApJL, 706, L150
Amorisco, N. C., & Evans, N. W. 2012, MNRAS, 419, 184
Battaglia, G., Irwin, M., Tolstoy, E., et al. 2008, MNRAS, 383, 183
Bell, E. F., Slater, C. T., & Martin, N. F. 2011, ApJL, 742, L15
Belokurov, V., Walker, M. G., Evans, N. W., et al. 2009, MNRAS, 397, 1748
Blais-Ouellette, S., Amram, P., & Carignan, C. 2001, AJ, 121, 1952
Brasseur, C. M., Martin, N. F., Macciò, A. V., Rix, H.-W., & Kang, X. 2011a, ApJ, 743, 179
Brasseur, C. M., Martin, N. F., Rix, H.-W., et al. 2011b, ApJ, 729, 23
Brooks, A. M., & Zolotov, A. 2012, arXiv:1207.2468
Bullock, J. S., Kravtsov, A. V., & Weinberg, D. H. 2000, ApJ, 539, 517
Bullock, J. S., Stewart, K. R., Kaplinghat, M., Tollerud, E. J., & Wolf, J. 2010, ApJ, 717, 1043
Chapman, S. C., Ibata, R., Irwin, M., et al. 2008, MNRAS, 390, 1437
Chapman, S. C., Ibata, R., Lewis, G. F., et al. 2005, ApJ, 632, L87
Chapman, S. C., Ibata, R., Lewis, G. F., et al. 2006, ApJ, 655, 255
Chapman, S. C., Peñarrubia, J., Ibata, R., et al. 2007, ApJL, 662, L9
Chapman, S. C., Widrow, L., Collins, M. L. M., et al. 2013, MNRAS, 430, 37
Chen, Y. Q., Zhao, G., & Zhao, J. K. 2009, ApJL, 706, L150
Conn, A. R., Ibata, R. A., Lewis, G. F., et al. 2011, ApJ, 740, 69
Courteau, S., Mateo, M., Olszewski, E. W., & Cook, K. H. 1999, ApJ, 526, 147
de Blok, W. J. G. 2005, ApJ, 634, 227
de Blok, W. J. G., & Bosma, A. 2002, A&A, 385, 816
de Blok, W. J. G., Bosma, A., & McGaugh, S. 2003, MNRAS, 340, 657
Dotter, A., Chaboyer, B., Jevremović, D., et al. 2008, ApJS, 178, 89
Ferguson, A. M. N., Ibata, M. J., Ibata, R. A., Lewis, G. F., & Tanvir, N. R. 2002, AJ, 124, 1452
Garrison-Kimmel, S., Rocha, M., Boylan-Kolchin, M., Bullock, J., & Lally, I. 2013, arXiv:1301.3137
Ho, N., Geha, M., Munoz, R. R., et al. 2012, ApJ, 758, 124
Holland, S., Fahim, G. M., & Richer, H. B. 1996, AJ, 112, 1035
Ibata, R., Chapman, S., Ferguson, A. M. N., et al. 2005, ApJ, 634, 287
Ibata, R., Irwin, M., Lewis, G., Ferguson, A. M. N., & Tanvir, N. 2001, Natur, 412, 49
Ibata, R., Martin, N. F., Irwin, M., et al. 2007, ApJ, 671, 1591
Ibata, R., Sollima, A., Nipoti, C., et al. 2011, ApJ, 738, 186

35
