Visual object pattern separation varies in older adults

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Young and nondemented older adults completed a visual object continuous recognition memory task in which some stimuli (lures) were similar but not identical to previously presented objects. The lures were hypothesized to result in increased interference and increased pattern separation demand. To examine variability in object pattern separation deficits, older adults were divided into impaired and unimpaired groups based on performance on a standardized serial list-learning task. Impaired older adults showed intact recognition memory, but were impaired relative to young and unimpaired older adults when identifying similar lure stimuli, demonstrating that object pattern separation varies in older adults.

Pattern separation is defined as a mnemonic process responsible for separating partially overlapping patterns of activation so that one pattern may be retrieved as separate from other similar patterns. Theoretical models have hypothesized that pattern separation may be supported by the hippocampus (Marr 1971; McNaughton and Nadel 1989; O’Reilly and McClelland 1994; Rolls and Kesner 2006; Myers and Scharfman 2009). The operation of a pattern separation mechanism may be fundamental in reducing interference among similar memory representations, thus enhancing memory accuracy. There is considerable evidence that the dentate gyrus (DG) and CA3 hippocampal subregions play a critical role in pattern separation (for reviews, see Kesner 2007; Gilbert and Brushfield 2009; Rolls 2010; Yassa and Stark 2011; Schmidt et al. 2012).

The DG is particularly susceptible to age-related changes in animals (Small et al. 2004; Patrylo and Williamson 2007) and humans (Small et al. 2002). In addition, age-related changes are evident in the perforant pathway in humans (Yassa et al. 2011b) and animals (Geinisman et al. 1992). Wilson et al. (2006) suggest that age-related changes in the DG and CA3 regions may be associated with memory accuracy. There is evidence that the DG may drive the network into previously stored attractor states, while weakening the processing of new information in the CA3 network.

Given the critical role of the DG in supporting pattern separation and the susceptibility of this region to age-related changes, recent studies have begun to examine the effects of aging on the efficiency of the pattern separation mechanism in humans. Pattern separation has been shown to be less efficient in older adults on tasks involving spatial locations (Yassa et al. 2011; Holden et al. 2012), visual objects (Toner et al. 2009; Yassa et al. 2011a; Stark et al. 2013), and temporal order of items in a sequence (Tolentino et al. 2012). Neuroimaging studies indicate that these age-related changes in pattern separation may be associated with functional and structural changes in the hippocampal network in older adults (Yassa et al. 2011a,b).

Although growing evidence indicates that pattern separation may be impaired in older adults, two recent studies suggest that there may be individual age-related variability in spatial pattern separation. Using different tasks, Stark et al. (2010) and Holden et al. (2012) found that when older adults were split into aged-impaired and aged-unimpaired groups based on standardized verbal learning test performance, the young adults and aged-unimpaired group performed significantly better than the aged-impaired group on trials hypothesized to tax pattern separation. However, very little is known about whether the differences reported in these studies are unique to spatial memory or whether the variability in pattern separation extends beyond the spatial domain. Only one study to our knowledge has investigated individual differences in pattern separation among older adults for visual object stimuli. Stark et al. (2013) found that pattern separation varied in older adults using an incidental encoding task. The purpose of the current study was to examine age-related variability in pattern separation efficiency for visual object information using a continuous recognition memory task that involved intentional encoding.

The present study used archival data from our laboratory that were included in a previous publication (Toner et al. 2009). The sample consisted of 20 nondemented older adults over 65 yr (M = 74.4 yr, SE 1.64) and 20 young adults (M = 19.15 yr, SE 0.30). Older adults were screened for dementia using the Dementia Rating Scale (DRS; Mattis 1976). For the current study, the older adult group was split into two groups based on...
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performance on the Hopkins Verbal Learning Test-Revised (HVLT-R; Benedict et al. 1998; Brandt and Benedict 2001). As defined by Holden et al. (2012), older-unimpaired (OU) participants (N = 8) scored within the normal range for young adults (ages 20–29 yr) on the delayed recall subtest of the HVLT-R (mean words recalled 11, SD 1.07), while older-impaired (OI) participants (N = 12) scored more than 1 standard deviation below these norms (mean words recalled 6.33, SD 1.5). It is important to note that the older-impaired adults were impaired relative to young adults on the HVLT-R but were not considered clinically impaired (defined as greater than 1.5 standard deviations below the norms for their age). HVLT-R scores were selected as the criterion to divide the older adults for several reasons. First, previous studies examining variability in pattern separation efficiency split older adults based on standardized verbal memory task performance (Stark et al. 2010, 2013; Holden et al. 2012). The utilization of a similar task in the present study allowed for more direct comparisons with prior studies. Second, given that pattern separation is a mnemonic process, it seemed most appropriate to split the group based on a test that assesses memory. Finally, serial list-learning tasks may be sensitive to medial temporal lobe function, which is implicated in pattern separation.

Demographic data for all groups and DRS scores for the older adult groups are provided in Table 1. There were no significant differences between the OU and OI participants on demographic variables or DRS scores. Although the OI group was older, had less education, and had lower average DRS scores compared to the OU group, none of these variables were found to correlate significantly with the pattern separation task (P > 0.10). In addition, analysis of variance revealed no significant differences between the OU and OI participants on a variety of neurocognitive tests, suggesting that general cognitive function did not differ significantly between the groups.

Participants completed a continuous recognition task developed by Kirwan and Stark (2007) during which they viewed pictures of everyday objects one at a time on a computer screen. Some objects were repeated across trials and some objects, labeled lures, were similar but not identical to objects previously presented. For each object, participants were asked to press a button to indicate whether the stimulus was: (1) new—the object had never been presented during the task; (2) old—the exact same object had been presented previously; or (3) similar—the object was similar, but not identical to one that had been presented previously during the task. Participants were administered six blocks of 108 stimuli. A given stimulus was repeated at most one time within a block and was never repeated across blocks.

The mean proportion of responses of new, old, and similar to first, repeated, and lure stimuli for the groups are displayed in Table 1. A 3 × 3 analysis of variance (ANOVA) with group (young, OU, OI) as the between-participant factor and stimulus (first, repeat, lure) as the within-participant factor was used to analyze correct responses. The analysis revealed a significant main effect of group, F(2,37) = 16.30, P < 0.001, ηp² = 0.43; a significant main effect of stimulus, F(2,74) = 98.81, P < 0.001, ηp² = 0.65; and a group × stimulus interaction, F(4,74) = 8.73, P < 0.001, ηp² = 0.11. A Newman–Keuls post-hoc comparison test of the interaction revealed that young and OU groups significantly outperformed the OI group in correctly identifying lures as similar. Effect sizes for group differences in the correct identification of lures were calculated using Cohen’s d. Effect sizes were large for the comparison of young vs. OI (d = 2.31) and OU vs. OI (d = 1.561). There were no significant group differences (P > 0.05) in correctly identifying first stimuli as new or repeated stimuli as old.

To examine the types of responses to lure stimuli, difference scores were calculated for each participant by subtracting the number of “old” responses to lure stimuli (false positive) from the number of “similar” responses to lure stimuli (correct response). A one-way ANOVA with group (Young, OU, OI) as the between-participant factor and difference scores as the dependent variable revealed a significant group difference, F(2,37) = 15.68, P < 0.001. A Newman–Keuls post-hoc comparison test revealed that young and OU were more likely to label a lure stimulus as similar, whereas OI were more likely to label a lure stimulus as old (Fig. 2). To further analyze types of errors committed by the OI group, a difference score was calculated subtracting the number of “new” responses to lure stimuli from the number of “old” responses to lures. A t-test with difference scores as the dependent variable revealed that OI participants labeled lure stimuli as old significantly more than new (t(11) = 5.92, P < 0.001).

These results reveal that young adults and OU significantly outperformed OI when correctly identifying lure stimuli as similar. Since there were no significant group differences in correctly identifying first stimuli as new or repeated stimuli as old, the group differences in correct responses to lures were not due solely to general recognition memory deficits. OI were more likely to commit false positive errors and label lure stimuli as old, providing evidence that pattern separation was less efficient in this group. These results suggest that deficits in visual object pattern separation may be variable in cognitively normal older adults. The current findings are consistent with three recent studies demonstrating individual differences in age-related pattern separation deficits for spatial (Stark et al. 2010; Holden et al. 2012) and visual object information (Stark et al. 2013). Inter-individual variability among aged individuals is evident in several aspects of memory, including recognition (Glisky et al. 1995; Christensen et al. 1999; Davidson and Glisky 2002; Wilson et al. 2002; Duarte et al. 2006) and immediate and delayed recall (Christensen et al. 1999; Wilson et al. 2002). However, the determinants of such variability are not well understood. Pattern separation is a mnemonic process that facilitates successful encoding, thus enhancing memory accuracy. The results of the current study, as well as of other recent studies demonstrating individual differences in pattern separation, suggest that efficiency of this mechanism may be a contributing factor in the variability in memory abilities in aged individuals.

Memory abilities have been linked to age-related neurobiological changes in the hippocampal formation. A recent longitudinal imaging study revealed that declines in episodic memory were associated with decreased hippocampal volume, as well as decreased activation in the left hippocampus, suggesting that structural and functional changes in the hippocampal formation are linked to memory decline (Persson et al. 2012). Small et al.
(2002) reported that 60% of an older adult sample had diminished MRI signal in at least one hippocampal subregion and this hippocampal dysfunction was associated with declines in memory ability. In addition, the authors demonstrated that DG dysfunction is associated with normal aging, whereas signal decline in the entorhinal cortex (EC) is indicative of a pathological process. However, even in healthy adults, shrinkage of the EC is associated with poorer memory performance (Rodrigue and Raz 2004). In addition, age-related structural changes in the perforant path, as well as functional changes in the DG/CA3 regions, are correlated with diminished pattern separation activity (Yassa et al. 2011b). Yassa et al. (2011b) suggest that these age-related changes in the hippocampal network, and the corresponding pattern separation
deficits, may lead to a shift from processing novel information to an over-reliance on retrieval of stored memory representations. The present finding that the OI group was more likely to identify lure stimuli as old rather than similar offers support for this hypothesis. The associations between these specific hippocampal subregions and age-related memory decline, in conjunction with the demonstrated role of these areas in supporting pattern separation, suggest that pattern separation efficiency may be an underlying mechanism subserving individual differences in memory decline in aging.

Although there is growing evidence to suggest that the human hippocampal subregions support pattern separation based on overlapping object features (Kirwan and Stark 2007; Bakker et al. 2008), there are data to suggest that perirhinal cortex also may play a role in pattern separation for visual objects. Lesion studies involving rats and monkeys indicate that lesions of the perirhinal cortex typically disrupt object recognition; however, hippocampal lesions produce variable results on object recognition tasks (Murray et al. 2000). Specifically, studies have shown that the perirhinal cortex may distinguish between visual objects with overlapping features to reduce feature ambiguity (Bussey et al. 2003, 2006; Gilbert and Kesner 2003; Norman and Eacott 2004; Bartko et al. 2007). However, there is some evidence to suggest that the hippocampus may play little role in disambiguating object features (Saksida et al. 2006). Aging studies have reported that total neuron numbers in rodents (Rapp et al. 2002) and cortical volumes in humans (Insauti et al. 1998) are largely preserved in the perirhinal cortex. However, researchers have postulated that age-related functional changes occur in perirhinal cortex in rodents (Moyer and Brown 2006) and humans (Ryan et al. 2012). Therefore, functional changes in the perirhinal cortex also may contribute to the decreased ability of older adults to identify lure stimuli as similar in the present study.

Future research should aim to identify the neurobiological underpinnings of individual differences in pattern separation in aging. It is important to identify whether there is corresponding inter-individual variability in dysfunction in specific hippocampal subregions and/or other regions such as the perirhinal cortex. Neurogenesis may play an important role in supporting mnemonic processes dependent on the DG, such as pattern separation (Clelland et al. 2009; Aimone et al. 2010; Deng et al. 2010, Sahay et al. 2011). Future investigations should examine potential associations between neurogenesis and individual differences in pattern separation abilities. In addition, evidence suggests that hippocampal subregions are differentially affected by normal and pathological aging processes (Braak and Braak 1996; West

**Figure 1.** Mean proportion of responses (+SE) of new, old, and similar to (A) first presentation of objects (FIRST), (B) repeated presentation of objects (REPEATED), and (C) objects that were similar but not identical to previously presented objects (LURE) for young, older-unimpaired (OU), and older-impaired (OI) adults.

**Figure 2.** Mean difference scores: proportion of “similar” responses to lure stimuli (correct response)—proportion of “old” responses to lure stimuli (false positive response) for young, older-unimpaired (OU), and older-impaired (OI) adults.
et al. 2000; Price et al. 2001; Small et al. 2002; Apostolova et al. 2010). It is unknown whether individual differences in pattern separation efficiency represent variability within the normal aging process or are indicative of early stages of a pathological process. If pattern separation deficits represent an early behavioral manifestation of future cognitive impairment, then tasks assessing pattern separation may be used in conjunction with standardized neuropsychological assessments to detect pathological changes. Finally, identification of older adults that perform similarly to young adults on these and other memory tasks provides a unique opportunity to further examine the factors involved in preserved memory function in aging. Future studies should aim to identify specific attributes of unimpaired older adults that may contribute to successful aging.

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