Machine learning and control engineering: 
The model-free case

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Abstract. This paper states that Model-Free Control (MFC), which must not be confused with Model-Free Reinforcement Learning, is a new tool for Machine Learning (ML). MFC is easy to implement and should be substituted in control engineering to ML via Artificial Neural Networks and/or Reinforcement Learning. A laboratory experiment, which was already investigated via today’s ML techniques, is reported in order to confirm this viewpoint

Keywords: Model-free control, intelligent proportional controllers, machine learning, reinforcement learning, supervised learning, unsupervised learning, artificial neural networks, half-quadrotor.

1 Introduction

The huge popularity today of Machine Learning (ML) is due to many beautiful achievements of Artificial Neural Networks (ANNs) (see, \textit{e.g.}, \cite{40,41,65}) and Reinforcement Learning (RL) (see, \textit{e.g.}, \cite{70}). Let us quote \cite{61}: “Reinforcement Learning is the subfield of machine learning that studies how to use past data to enhance the future manipulation of a dynamical system. A control engineer might be puzzled by such a definition and interject that this precisely the scope of control theory. That the RL and the control theory communities remain practically disjoint has led to the co-development of vastly different approaches to the same problems. However, it should be impossible for a control engineer not to be impressed by the recent successes of the RL community such as solving Go \cite{66}.” Many concrete case-studies have already been investigated: see, \textit{e.g.}, \cite{49,18,17,13,16,14,17,21,22,31,37,43,44,46,58,57,64,65,68,74,75,77,78,81,82,83,85,86,87}. Although those works are most promising, they show that ANNs and RL have perhaps not provided in this field such stunning successes as they did elsewhere.
Remark 1. The connection of RL with optimal control is known since ever (see, e.g., [15, 37, 61]). According to [47, 48] tools stemming from advanced control theory should enhance RL in general.

This communication suggests another route: Model-Free Control (MFC) in the sense of [25].

Remark 2. The meaning of Model-Free Reinforcement Learning is quite distinct. In model-free RL there is no transition probability distribution, i.e., no model (see, e.g., [69, 70]). Q-learning is an example which has been used several times in control engineering.

MFC, which is easy to implement both from software [25] and hardware [32] viewpoints, leads to many acknowledged applications (see the bibliographies in [25], [6] for most references until 2018). The relationship with ML is sketched below.

Consider a system $S$ with a single input $u$ and a single output $y$. Under rather weak assumptions $S$ may be approximated (see [25] and Section 2) by the ultra-local model:

$$
\dot{y}(t) = F(t) + \alpha u(t) \tag{1}
$$

where $F$ encompasses not only the poorly known structure of $S$ but also the disturbances. Since $\alpha$ is a constant that is easy to nail down (see Section 2.2), the main task is to determine the time-dependent quantity $F(t)$. A real-time estimate $F_{\text{est}}(t)$ is given thanks to a new parameter identification technique [26, 27, 67] by the following integral of the input-output data

$$
F_{\text{est}}(t) = - \frac{6}{\tau^3} \int_{t-\tau}^{t} \left[ (\tau - 2\sigma)y(\sigma) + \alpha \sigma (\tau - \sigma)u(\sigma) \right] d\sigma \tag{2}
$$

where $\tau > 0$ is small. Formula (2), which ought to be viewed as a kind of unsupervised learning (see, e.g., [63]) procedure, takes into account the time arrow: the structure of $S$ and especially the disturbances might be time-varying in an unexpected way. Moreover the unavoidable corrupting noises are attenuated by the integral, which is a low pass filter (see Remark 3). Associate the feedback loop [25]

$$
u = - \frac{F_{\text{est}} - \dot{y}^* + K_P e}{\alpha} \tag{3}
$$

where

- $y^*$ is a reference trajectory,
- $e = y - y^*$ is the tracking error,
- $K_P \in \mathbb{R}$ is a gain.

\footnote{Some applications are patented. Others have been published more recently (see, e.g., [127, 181, 19, 20, 25, 29, 30, 35, 50, 55, 56, 60, 62, 64, 71, 72, 73, 76, 79, 84, 86]).}
It has been baptised intelligent proportional controller (iP), already some time ago [24]: this unsupervised learning permits not only to track the reference trajectory but also to limit the effects of the disturbances and of the poor system understanding (see Section 2.3 for further details). Note that ANNs and RL, and the corresponding methods from computer sciences and mathematics, are not employed.\footnote{It is perhaps worth mentioning that some other fields of computer sciences might benefit from MFC (see, e.g., [10,33]).}

In order to support our viewpoint a lab experiment has been selected. A half-quadrotor is available to one of the authors (C.J.). Moreover quadrotors and half-quadrotors have been already examined via ANNs and RL; see, e.g., [31,39,59,77]. Our results are not only excellent but also easy to obtain. The interested reader is invited to compare with the above references. It has been moreover shown [20] that the performances of MFC with respect to quadrotors are superior to those of PIDs (see, e.g., [4,5]).\footnote{Numerous other references do not use any traditional AI techniques.}

This communication is organized as follows. MFC is reviewed in Section 2. Section 3 discusses the lab experiment. Some concluding remarks may be found in Section 4.

\section{MFC as a ML technique}

\subsection{The input-output system as a functional}

Consider for notational simplicity a SISO system, \(i.e.,\) a system with a single control variable \(u(t)\) and a single output variable \(y(t)\), where \(t \geq 0\) is the time. Even without knowing any “good” mathematical model we may assume that the system corresponds to a functional (see, e.g., [36]), \(i.e.,\) a function of functions: for any \(t \geq 0\)

\[ y(t) = \mathcal{F}(u(\tau) \mid 0 \leq \tau \leq t) \]  

\(\mathcal{F}\) depends not only on initial conditions at \(t = 0\), but also on the unavoidable disturbances.

\subsection{The ultra-local model}

It has been demonstrated [25] that, under mild assumptions, the input-output behavior [1] may be well approximated by the ultra-local model:

\[ \dot{y}^{(n)}(t) = F(t) + \alpha u(t) \]

where the order \(n \geq 1\) of derivation is in all known examples equal to 1 or 2. In most concrete case-studies, \(n = 1\). The case \(n = 2\) arises, for instance, with weak frictions [25] (see, e.g., [49] for a concrete case-study). Consider from now on only the case \(n = 1\), \(i.e.,\) Equation [1], which works well in Section 3.

\[ Proportional-Integral-Derivative (PID)\ controllers ought to be regarded as the “bread and butter” of control engineering!\]
The time-dependent quantity $F$ is not only encompassing the internal structure of the system, which may be poorly known, but also the disturbances. Write $F_{\text{est}}$ its estimate which is derived in Section 2.4.

The constant $\alpha \in \mathbb{R}$ is chosen by the practitioner such that the three terms in Equation (1) are of the same magnitude. A precise determination of $\alpha$ is therefore meaningless. In practice $\alpha$ is easily chosen via two possible approaches:

- the absolute value $|\frac{\alpha u(t)}{y(t)}|$ is not too far from 1,
- trial and error, i.e., a kind of supervised learning (see, e.g., [63]).

### 2.3 Intelligent proportional controllers

Close the loop in Equation (1) with the iP (3). Equations (1) and (3) yield

$$\dot{e} + K_P e = F - F_{\text{est}}$$

If the estimation $F_{\text{est}}$ is “good”: $F - F_{\text{est}}$ is “small”, i.e., $F - F_{\text{est}} \simeq 0$, then $\lim_{t \to +\infty} e(t) \simeq 0$ if $K_P > 0$. It implies that the tuning of $K_P$ is quite straightforward. This is a major benefit when compared to the tuning of “classic” PIDs (see, e.g., [4, 5]).

### 2.4 ML via the estimation of $F$

Any function, for instance $F$ in Equation (1), may be approximated under a weak integrability assumption by a piecewise constant function (see, e.g., [12]). The estimation techniques below are borrowed from [26, 27, 67].

**First approach** Rewrite Equation (1) in the operational domain (see, e.g., [80]):

$$sY = \frac{\Phi}{s} + \alpha U + y(0)$$

where $\Phi$ is a constant. We get rid of the initial condition $y(0)$ by multiplying both sides on the left by $\frac{d}{ds}$:

$$Y + s \frac{dY}{ds} = -\frac{\Phi}{s^2} + \alpha \frac{dU}{ds}$$

Noise attenuation is achieved by multiplying both sides on the left by $s^{-2}$. It yields in the time domain the real-time estimate Formula (2) thanks to the equivalence between $\frac{d}{ds}$ and the multiplication by $-t$, where $\tau > 0$ might be quite small. This integral, which is a low pass filter, may of course be replaced in practice by a classic digital linear filter.

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8 See, e.g., in [72] an optimization procedure, which, in some sense, is closer to today’s viewpoint on ML.
Second approach Close the loop with the iP (3). It yields:

\[ F_{\text{est}}(t) = \frac{1}{\tau} \left[ \int_{t-\tau}^{t} (\dot{y}^* - \alpha u - K_{pe}) \, d\sigma \right] \]

Remark 3. Noises, which are usually described in engineering and, more generally, in applied sciences via probabilistic and statistical tools, are related here to quick fluctuations around 0 [23]. The integral of any such noise over a finite time interval is close to 0. The robustness with respect to corrupting noises is thus explained. See, e.g., [11,67] for concrete applications in signal processing where the parameter estimation techniques of [26,27,67] have been employed.

2.5 MIMO systems

Consider a multi-input multi-output (MIMO) system with \( m \) control variables \( u_i \) and \( m \) output variables \( y_i, i = 1, \ldots, m, m \geq 2 \). It has been observed in [38] and confirmed by all encountered concrete case-studies (see, e.g., [73]), that such a system may usually be regulated via \( m \) monovariable ultra-local models:

\[ y_i^{(n_i)} = F_i + \alpha_i u_i \]  

where \( F_i \) may also depend on \( u_j, y_j \), and their derivatives, \( j \neq i \).

3 Experiments: A half-quadrotor

3.1 Process description

Our half-quadrotor (see Fig. 1), called AERO, is manufactured by Quanser [9]. Two motors driving the propellers, which might turn clockwise or not, are controlling the angular positions: the azimuth (horizontal) velocity and pitch (vertical) position of the arms. Outputs \( y_1 \) and \( y_2 \) are respectively measures of the azimuth velocity (rad/ms) and pitch position (rad). Write \( v_i, i = 1, 2 \), the supply voltage of motor \( i \), where \(-24v \leq v_i \leq 24v \) (volt). Measures and control inputs are updated each 10ms.

3.2 Control

It is clear that \( y_i, i = 1, 2 \), is mainly influenced by \( v_i \). Equations (5) and (3) become

\[ \dot{y}_i = F_i + \alpha_i u_i \]  

\[ u_i = F_{i,\text{est}} - \dot{y}^* + K_{P,i} e_i \]

The control variable \( u_i \) in Equation (6) is defined by

\[ u_i = -\frac{F_{i,\text{est}} - \dot{y}^* + K_{P,i} e_i}{\alpha_i} \]

9 See the link https://www.quanser.com/products/quanser-aero/
Fig. 1. The Quanser AERO half-quadrotor

\[ \text{if } u_i > 0, \text{ then } v_i = 10 + u_i, \]
\[ \text{if } u_i < 0, \text{ then } v_i = -10 + u_i. \]

In Equations (7)-(8), set $\alpha = 0.001$, $K_{P,1} = 0.5$, $\alpha_2 = 5$, $K_{P,2} = 500$. Everything is programmed in C# and stored in the server.

3.3 Experiments

**Nominal half-quadrotor** Consider two scenarios:

- scenario 1 – simple reference trajectory (see Fig. 3 and 4),
- scenario 2 – complex reference trajectory (see Fig. 5 and 6).

The tracking is excellent in both cases in spite of the rotating blades, the gyroscopic effects, and the frictions, which are all taken into account by $F_i$. 
Adding a mass  Fig. 2 shows that a mass of 4 grams is added. It is taken into account by $F_i, i = 1, 2$. There is no new calibration. Keep the previous scenarios:

- scenario 3 – simple reference trajectory (see Fig. 7 and 8),
- scenario 4 – complex reference trajectory (see Fig. 9 and 10).

The tracking does not deteriorate.

4 Conclusion

Of course further studies are needed in order to support the thesis of this paper. MFC might not be able to provide a satisfactory fault detection\textsuperscript{10} The rôle of ANNs and RL might then be compelling (see, e.g., \textsuperscript{45}).

The epistemological connections of MFC with other existing approaches in AI (see, e.g., \textsuperscript{63}), Wiener’s cybernetics for instance, will be analyzed elsewhere.

\textsuperscript{10} See \textsuperscript{25,38} for fault accommodation.
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Fig. 3. Scenario 1: Azimuth
Fig. 4. Scenario 1: Pitch

(a) Pitch position (blue --), reference trajectory (red --)

(b) Control $u_2$
Fig. 5. Scenario 2: Azimuth

(a) Azimuth velocity (blue −−), reference trajectory (red −−)

(b) Control $u_1$
(a) Pitch position (blue −−), reference trajectory (red −−)

(b) Control $u_2$

Fig. 6. Scenario 2: Pitch
Model-free control

**Fig. 7.** Scenario 3: Azimuth

(a) Azimuth velocity (blue −−), reference trajectory (red −−)

(b) Control $u_1$
Fig. 8. Scenario 3: Pitch

(a) Pitch position (blue $\cdash\cdash$), reference trajectory (red $\cdash\cdash$)

(b) Control $u_2$
(a) Azimuth velocity (blue \(\cdots\)), reference trajectory (red \(\cdots\))

(b) Control \(u_1\)

Fig. 9. Scenario 4: Azimuth
Fig. 10. Scenario 4: Pitch

(a) Pitch position (blue --), reference trajectory (red --)

(b) Control $u_2$