Laser-driven high-quality positron sources as possible injectors for plasma-based accelerators

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The intrinsic constraints in the amplitude of the accelerating fields sustainable by radio-frequency accelerators demand for the pursuit of alternative and more compact acceleration schemes. Among these, plasma-based accelerators are arguably the most promising, thanks to the high-accelerating fields they can sustain, greatly exceeding the GeV/m. While plasma-based acceleration of electrons is now sufficiently mature for systematic studies in this direction, positron acceleration is still at its infancy, with limited projects currently undergoing to provide a viable test facility for further experiments. In this article, we study the feasibility of using a recently demonstrated laser-driven configuration as a relatively compact and inexpensive source of high-quality ultra-relativistic positrons for laser-driven and particle-driven plasma wakefield acceleration studies. Monte-Carlo simulations show that near-term high-intensity laser facilities can produce positron beams with high-current, femtosecond-scale duration, and sufficiently low normalized emittance at energies in the GeV range to be injected in further acceleration stages.

Since the experimental discovery of the positron in 1932, positron beams have played a major role in experimental physics, not only for fundamental studies but also for their wide range of practical applications, which include medicine and material science. Sub-relativistic or mildly relativistic positrons are naturally emitted by elements undergoing β⁺-decay, a widely used source for positron annihilation spectroscopy and positron emission tomography. On the other hand, ultra-relativistic positron beams are widely used in experimental particle and nuclear physics, predominantly in electron-positron colliders. The current record for the highest centre-of-mass energy in an electron-positron collider belongs to the recently dismissed LEP at CERN, able to achieve up to 209 GeV. Recent proposals for the next generation of particle colliders aim at increasing this energy, eventually reaching the TeV-scale centre-of-mass energy. For example, the International Linear Collider (ILC) and the Compact Linear Collider (CLIC) aim, in their first stage of implementation, to achieve 250 GeV and 380 GeV, respectively.

Increasing collider energies to hundreds of GeV would allow precision studies of the Higgs boson and the top quark, such as the possibility of the Higgs boson being a composite particle and its coupling with the top quark and itself, besides providing hints as to why it condenses giving a non-zero vacuum expectation value. Furthermore, breaking the TeV barrier would allow for searches beyond the Standard Model of particle physics. Besides the challenging requirement of accessing TeV-scale centre-of-mass energies, it is also necessary to create collisions at extremely high luminosity, since the typical cross sections involved scale as the inverse of the energy squared. For this reason, ILC and CLIC are aiming for luminosities greater than $10^{34} \text{cm}^{-2} \text{s}^{-1}$, well beyond the $10^{31} \text{cm}^{-2} \text{s}^{-1}$ previously achieved at LEP.

Conventional electron-positron colliders rely on established radio-frequency technology, which guarantees a maximum accelerating gradient at the level of tens to a 100 MV/m. This field is limited by the dielectric breakdown of the materials involved, implying that TeV energies can only be reached after tens to hundreds of km of acceleration. The sheer scale of these machines is thus a fundamental limiting factor in the development of lepton colliders justifying research into alternative acceleration schemes that can provide similar performance but in a more compact configuration. Plasma-based wakefield acceleration is arguably one of the most promising, since it can sustain accelerating fields well beyond the GeV/m, with experimentally demonstrated fields up to 100 GeV/m. Recent promising results in this area include, for instance, the demonstration of energy doubling of...
a 42 GeV electron beam in less than one meter of plasma, a 2 GeV energy gain of a positron beam in one metre of plasma, and the laser-driven acceleration of electrons up to 8 GeV in only 20 cm of plasma. Thanks to its fast-paced development, particle-driven wakefield acceleration is now actively pursued in large-scale projects, including AWAKE at CERN and FACET at SLAC (together with its current upgrade, FACET-II). On the other hand, laser-driven wakefield is currently studied only in relatively small University-scale laboratories even though the physics of laser-driven wakefield acceleration is in principle sufficiently mature to widespread its use to larger-scale applications. One example in this direction is the European funded project EuPRAXIA, which aims at building a plasma-based electron accelerator of industrial quality able to accelerate, in a stable and consistent manner, narrow-band and high-current electron beams with a maximum energy of 5 GeV.

Developing plasma based accelerator technology to the level required by TeV-scale colliders represents a major challenge requiring progress in many fields as outlined in the recently published US roadmap for advanced accelerators. In a nutshell, a possible proposal is to use multi-staged wakefields, following promising results in proof-of-principle experiments of double-staged electron acceleration. Even though the field of plasma-based electron acceleration is advancing fast, experimental studies of positron acceleration in a plasma is of a more challenging nature, due to the difficulty of providing an injector of suitable quality that can be, for instance, synchronised with the positron-accelerating region of a wakefield. To date, only the proposed upgrade of FACET will be able, in the near future, to provide a source of ultra-relativistic positrons suitable for test studies of subsequent wakefield acceleration. In preliminary studies, including those in FACET-I, two alternative methods have been studied. The first option uses an electron beam as a driver and a positron beam as a witness, both propagating inside a hollow channel to avoid the positron-defocussing fields. The temporal synchronisation is ensured by propagating the electron drive through a thin converter to generate the positron beam. Alternatively, the self-loaded plasma wakefield acceleration has been proposed, in which a high-charged positron beam is propagated through a hollow channel. The front of the positron bunch is in charge of generating the wakefield, whose accelerating fields are experienced by the back of the bunch. Providing positron beams of suitable quality to study these acceleration schemes is indeed extremely challenging, with effectively only FACET-II as a viable facility proposed to date. However, recent experimental results on laser-based generation of high-quality ultra-relativistic positrons are suggesting an alternative pathway towards this goal. For instance, the generation of fs-scale and narrow divergence positron beams in a plasma-based configuration has been reported recently. In a nutshell, the positrons are generated as a result of a quantum cascade initiated by a laser-driven electron beam propagating through a high-Z solid target. For sufficiently high electron energy and thin converter targets, the generated positrons present properties that resemble those of the parent electron beam, hence the fs-scale duration, mrad-scale divergence, and small source size. The maximum positron energy attainable in this scheme is naturally dictated by the peak energy of the parent electron beam. Positrons with energy up to 0.5 GeV were produced in recent experiments. These beams present unique advantages for being injected in further wakefields, when compared to more conventional sources. For instance, they have durations comparable to the positron-accelerating region of a wakefield and are naturally synchronised with a high-power laser. However, other characteristics still need to be carefully optimised, such as their non-negligible normalised emittance and the relatively low charge. Providing a high-quality source of ultra-relativistic positrons is however of paramount importance for the development of plasma-based accelerators of positrons, to date an area of research predominantly of a theoretical nature (see, for instance, ref.). In this paper, we report on an extensive numerical study devoted to define precisely the main properties of laser-driven positrons and assess their suitability to be further transported and manipulated in order to act as a seed for further wakefield-based acceleration stages. In this study, we assume three main ranges of parameters for the primary electron beam. In the first range, we consider typical electron parameters obtainable by 100 TW commercially-available laser systems (maximum electron energy of 1 GeV). In the second, we assume state-of-the-art electron beam properties, similar to the characteristics reported in ref. and planned to be achieved by EuPRAXIA (maximum electron energy of 5 GeV). Finally, we consider near-term beam properties expected to be achieved by the next generation of ultra-high intensity laser systems, such as the Extreme Light Infrastructure Nuclear Pillar (maximum electron energy of 20 GeV). Our simulations show that high current (exceeding the kA) positron beams with sufficiently low emittance and high density can be generated, providing a firm baseline for the design of a test facility dedicated to optimising positron beam manipulation and further acceleration.

Results

Spatial and spectral properties of the positrons at source. In order to assess the main characteristics of the positron beam, we simulated the propagation of an ultra-relativistic electron beam through a high-Z solid target, using the Monte-Carlo scattering code FLUKA. (See Methods for further details). For its practical simplicity, we simulate lead as a converter target and we assume a length of the order of two radiation lengths \(2L_{rad} \approx 1 \text{ cm for lead}\). This length is the one that maximises the number of escaping positrons, for any defined set of parameters of the incoming electron beam. In order to make the obtained characteristics of the positron beam independent from those of the parent electrons, we assume a pencil-like electron beam with a point-like source and zero temporal duration. For a realistic electron beam, it is thus only necessary to convolute the parameters of the parent electrons with those of the positrons. In each simulation, a bunch of 10^6 primary electrons interacts with the high-Z target creating a positron beam. The main properties of the positron beams that we consider are: source size \(d\), divergence \(\theta_{div}\), temporal duration \(\tau\), energy \(E\), geometrical emittance \(\varepsilon\), and normalised emittance \(\sigma\). These properties are tracked at source; i.e. at their exit of the converter through its rear side. As mentioned in the introduction, three different electron energies are chosen: \(E_{el} = 1, 5, \text{ and } 20 \text{ GeV}\). For each energy, we simulated a primary electron beam with a Gaussian spectrum centred around \(E_0\) and a standard deviation \(\sigma_{E} = 5\%E_0\). These three energies are chosen in order to represent the typical performance of a laser-driven electron accelerator employing a commercial laser system, state-of-the-art high-intensity lasers, and the next generation of high-intensity lasers (such as the Extreme Light Infrastructure (ELI)), respectively. For the 5 GeV
case, it is also worth noticing that this is the baseline energy of the EuPRAXIA project\(^{16}\). For the number of positrons escaping the solid target, we generally assume that the primary electron beam carries a charge of 100 pC. However, the number of positrons is directly proportional to the number of electrons in the parent beam\(^{37}\), allowing for a simple rescaling of the results for different initial electron charges. The spectra of the positrons escaping the converter are depicted in Fig. 1. As expected from the quantum cascade in the solid, the spectra present a monotonic shape with a maximum energy corresponding to the energy of the parent electron beam. The characteristic spectral shape, as previously explained in the literature\(^{36}\), is the result of the combination of the power spectrum of the radiation produced via Bremsstrahlung and pair production. However, it is worth noticing that a 100 pC electron beam, as routinely obtainable in a laser wakefield accelerator, is able to generate a significant number of positrons, even in a narrow energy slice. For instance, assuming EuPRAXIA-like parameters, up to \(10^{11}\) positrons with energy exceeding 100 MeV can be generated, with up to \(6 \times 10^{9}\) positrons in a 5% bandwidth around 1 GeV, corresponding to a charge of approximately 1 pC. This number raises to \(1.8 \times 10^{10}\) (charge of 3 pC) if an initial electron beam with an energy of 20 GeV is considered. As a further comment, it must be noted that the spectrum of the generated positrons is virtually insensitive to the spectrum of the parent electron beam. As higher electron charges can be obtained from laser-based configurations when looser conditions are imposed on the spectral bandwidth, using high-charge broadband electron beams may be preferable to enhance the positron yields generated. If we assume a 1 nC electron beam with a broadband spectrum up to 5 GeV, we can then obtain up to \(10^{10}\) positrons in a 5% bandwidth around 1 GeV.

This is a sizeable positron beam that could in principle be injected in further stages of laser-driven or particle-driven wakefield acceleration, provided that the beam possesses sufficient spatial quality. In particular, it is necessary to assess the source size, the divergence, and the emittance of the beam. Due to the generation of the positrons throughout the converter, the definition of the source is somewhat ambiguous. In our case, we define the real source size as the size of the positron beam at the rear surface of the converter and a virtual source size corresponding to the waist of the beam obtained by back-tracking the generated positrons.

The positron beam profile at the exit of the converter target is depicted in Fig. 2(a) for the case of a 5 GeV initial electron beam, accounting for all the positrons emitted independent of their energy or time of arrival. As it can be seen, the positron beam exhibits a smooth profile, in agreement with previous experimental observations\(^{30}\). The source size of the overall beam can be estimated to be \(\sim 33\, \mu\text{m}\), given by the radius or Half-Width-at-Half-Maximum of the distribution. However, the source size is energy-dependent with the spatial distribution being well-approximated by a Lorentzian distribution: \(N_{\text{ex}} \propto k/[\pi \sigma_{\pi}(1 + (x/\sigma_{\pi})^2)]\), where \(\sigma_{\pi}\) is the HWHM, and \(k\) is a normalisation constant (see Fig. 2(b)), with smaller sizes \(\sigma_{\pi}\) for higher energies (see Fig. 2(c)). As an example, 1 GeV positrons have a source size of around 20 microns (10 microns) if a parent 5 GeV (20 GeV) electron beam is assumed. The virtual source size is found to be about 16 micron (7.5 micron), placed inside the converter at a distance of 1.6 mm (0.8 mm) from its rear surface. This source size arises from assuming a pencil-like electron beam with a point-like source. In order to compute the realistic positron source size one would then need to convolute these results with the intrinsic beam size of the specific electron beam used. However, laser-driven electron beams typically have a source size in the micron range\(^{37}\) and divergences in the mrad range\(^{37}\). Thanks to the compactness of the positron-generation schemes, where the converter is closely-coupled to the plasma source, the electron beam size will account for a few microns on the front face of the converter, inducing only small corrections to the results reported here.

Similarly, the divergence of the positrons is seen to decrease for increasing positron energies, as depicted in Fig. 3. At 1 GeV the positrons have a divergence of the order of 10 mrad, which decreases further down to 3 mrad at 5 GeV. The divergence is seen to scale with the positron energy as \(\propto E^{-0.87}\), in good qualitative agreement with the Rossi-Greisen formula\(^{38}\) routinely used in accelerator physics. Again this divergence should be convoluted with the divergence of the primary electron beam, inducing a small correction, in the mrad range.
Temporal properties of the positrons at source. A defining feature of laser-driven electron beams is their short temporal duration, down to even the femtosecond-scale. Such a short duration is in principle achievable by radiofrequency accelerators, but at the cost of implementing complex beam slicing devices. It is thus to be expected that positrons generated from such electron beams will present similarly short durations. In order to extract the temporal duration of the positron beam at source, a specific add-on code was written in the source files of FLUKA (see Methods). The parent electrons are considered to be produced simultaneously, with the code taking into account the birth time and time of flight of the positrons until their exit through the rear surface of the converter. Obtained beam durations are shown in Fig. 4. Frame a) depicts the temporal distributions of positrons of different energy. Each distribution resembles a log-normal distribution with different variances. As intuitively expected, higher positron energies correspond to shorter beam durations, of the order of approximately 1 fs (longitudinal size of 300 nm) at 1 GeV for a 5 GeV parent electron beam. This effectively implies that the 1 GeV positron beams will have virtually the same duration as the primary electron beam. Assuming a realistic electron beam with a duration of 5 fs, we obtain a longitudinal size of the positron beam of the order of $\sigma_z \approx 1.5 \mu m$. 

Figure 2. Energy-dependent source-size of the positron at the exit of the converter target. (a) Spatial distribution of the entire positron beam at the rear surface of the converter. (b) Transverse distribution of the positrons for different positron energies, generated by a 5 $\pm$ 5% GeV electron beam, fitted by Lorentzian distributions of different width. (c) Extracted energy-dependent size of the real source of the positrons for different parent electron beam energies. The source size of the positrons is seen to scale approximately as the cubic root of their energy (as fitted by the red and black dashed lines).
This value is much smaller than the one proposed for FACET-II (10 μm) and indeed extremely useful for high-energy applications. For instance, a short longitudinal size is highly desirable for injection in additional wakefield acceleration stages. The extremely small positron-accelerating region, of a few microns, in plasma wakefield accelerators have led to alternative schemes being investigated, such as self-loaded PWFA. In

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**Figure 3.** Energy-dependent divergence of the positrons at the exit of the converter target. Different colours correspond to different energies of the primary electron beam. At multi-GeV, the divergence of the positrons scales approximately as the inverse of their energy (fit shown by the black dashed line), in good qualitative agreement with the Rossi-Greisen formula (red dashed line).

**Figure 4.** Temporal properties of the positron beam at source. (a) Temporal profile of the positrons of energy 250, 500, 1000, and 2500 MeV, produced from the interaction of a 5 GeV electron beam with a 1 cm-thick Pb target. The points are well fitted by a log-normal distribution. (b) Duration of the positron beam as a function of their energy. (c) Peak current of the positrons contained within each 5% energy bin.
SL-PWFA, the front of a long, high-charge positron beam drives a wakefield, which accelerates the positrons contained in the back of the bunch, in a positron-accelerating region larger than in the regular electron-driven wakefield. However, such a mechanism requires very large positron charges in order to generate the wakefield, while only a small fraction of these positrons are actually accelerated. Furthermore, the extension of the accelerating region comes at the cost of a significant reduction of the accelerating field. The intrinsically-short durations of laser-driven positron beams would allow the positron acceleration in the original wakefield produced by a laser or an electron drive beam, reducing the number of stages required for high-energy applications.

Moreover, a short beam duration is recommended in order to minimise beam disruption in high-energy electron-positron collisions, as caused by beam focussing induced by the electromagnetic fields of the other beam. The beam disruption parameter is in fact directly proportional to the beam longitudinal size:\(^{40}\)

\[
D_{x,y} \approx \frac{2\gamma N \sigma_{x,y}}{\gamma \sigma_{x,y}^2 (\sigma_x + \sigma_y)},
\]

where \(r_e\) is the classical electron radius, \(\gamma\) is the particle Lorentz factor, \(N\) is the number of particles in a beam, and \(\sigma_{x,y}\) are the transverse dimensions of the beam.

Moreover, a short longitudinal size of the beam is also desirable in order to minimise beamsstrahlung, one of the main sources of background noise in high-energy colliders\(^{41}\). In its quantum regime, the number of photons generated via beamsstrahlung scales as \(n_{\text{ph}} \propto \sigma_{\text{1s}}^{1/3}\) and the number of pairs produced coherently \(n_{\text{coh}} \propto \sigma_{\text{1s}}^{2/3}\).

Finally, a short beam duration naturally translates into a high peak current of the beam (Fig. 4c). In a 5% slice centered around 1 GeV, a 5 GeV, 100 pC electron beam can generate a positron current exceeding the kA, albeit these values consider an instantaneous electron source and the actual current would be slightly reduced when taking into account the duration of the laser-driven electron beam. Even though one must note that a high current is not explicitly required in liner colliders, this characteristic is still of great interest for other applications in material science.

**Emittance of the positrons at source.** The positrons generated inside the converter are emitted in a beam-like fashion. Such a beam can be described, in a first approximation, by its source size and divergence. However, the most important parameter to characterise the spatial quality of a beam is arguably its emittance. The emittance is a measure of the volume of the particle beam in phase-space, and defines the ease for beam transportation using magnetic fields, as well as being the main parameter in conjunction with the current defining the brightness of the beam. The emittance is mathematically defined as \(\varepsilon_x = \sqrt{(\langle x^2 \rangle - \langle x \rangle^2)}\), where \(x\) is the position of the particles and \(x'\) its divergence. Typically, the emittance is defined for particles within a narrow energy range (monoenergetic approximation) and low angular divergence (paraxial approximation), which allows to define the normalised emittance as \(\varepsilon = \gamma \beta \varepsilon_c\), where \(\gamma\) is the particle Lorentz factor and \(\beta\) its velocity normalised to the speed of light in vacuum. As an example, the phase-space of positrons of energy 1.00 ± 0.05 GeV leaving the converter is shown in Fig. 5(a), as generated from the interaction of a 5 GeV electron beam. The emittance in this case corresponds to the area of the ellipse defined by the rms of the distribution, depicted in Fig. 5(a) by the black, dash-dotted ellipse. With that, a geometrical emittance of \(\varepsilon_x = 0.1\pi\) mm mrad is obtained (normalised emittance \(\varepsilon_x = 200\pi\) mm mrad). Given the strong dependence of both source size and divergence on the positron energy considered, the emittance is expected to follow a similar trend. The scaling of the normalised emittance with the positron energy bin is shown in Fig. 5(b), showing the data points to closely follow a power-law function. Comparing the trends, the emittance of the generated positrons with a given energy by a 1 GeV parent electron beam is about ~50% greater than for the exemplary 5 GeV electron beam, while a reduction of ~20% is achieved in the case of the 20 GeV parent beam.

**Discussion**

The main properties of positrons generated from laser-driven electrons have been shown in the previous sections. These characteristics can be directly compared with those obtainable with more conventional generation schemes and with the requirements for injection in laser-driven and particle-driven wakefield acceleration stages. We take FACET-I and FACET-II as representative examples of state-of-the-art particle-driven wakefield facilities and this comparison is shown in Table 1.

As one can see, the main drawback for the use of laser-driven sources is given by the lower number of positrons in the beam, limited to a few pC of charge for realistic charges of the parent electron beam (100 pC – 1 nC). This charge is two orders of magnitude lower than that attainable with FACET, and up to three orders of magnitude lower than the charges in conventional accelerators, such as the Stanford Linear Collider (SLC, 1.6 nC), Large Electron Positron collider (LEP, 240 pC), or estimated for the International Linear Collider (ILC, 3.2 nC). The main reason for the lower charge is the significantly lower electron charge attainable via LWFA compared to the 10s–100s nC of charge in conventional accelerators in the other cases. However, it should be noted that few pC charges is sufficient for most applications (including cooling and acceleration studies for positrons towards colliders), particularly with the advances in high power lasers towards higher repetition rates. The main bottleneck to reach higher repetition rates in high power lasers has been the cooling of the lasing medium, due to the use of white flashlamps as pumps. The use of diodes with wavelength in the absorption band for the laser emission will allow for higher repetition rates. For instance, the DiPOLE project has recently demonstrated a stable system delivering 10 J laser pulses at 10 Hz. The design is scalable and demonstration of 100 J laser pulse energy at 10 Hz is forthcoming, eventually aiming for a 1 kJ 10 Hz laser. The need for the development of 1 kHz high power lasers is also identified in the US roadmap for future novel accelerators. Such high repetition rates will help compensating the lower single-shot charge by providing a greater time-averaged charge. It should be noted that, in the context of closely-coupled experiments and higher repetition rate lasers, additional measures may need to be implemented.
to protect the converter from damage by the laser and the radiation generated. For the former, the converter can be protected from the intense laser by deviating it using thin foil in a tape-like configuration, without significantly modifying the properties of the generated electron beam. For the latter, the propagation of a high-current electron beam through the converter will deposit a significant amount of energy in the form of heat. Several options, already in use at conventional positron accelerators, are envisaged to prevent damage, such as rotating converters or active cooling.

Furthermore, the total charge in the beam can be increased significantly simply by considering a larger energy bandwidth. For example, the final stage of LEP used positrons accelerated by the pre-linac with energy in the range $90 \pm 1\% \text{ MeV}$, and SLC could accelerate up to 20% of the positrons initially contained in the energy range $11 \pm 80\% \text{ MeV}$. Considering both solutions, the time-averaged charge of LWFA-driven positrons could reach values of hundreds of $\text{pC}$ per second, comparable to that of the FACET projects.

As shown in Table 1, the normalised emittance of the LWFA-based positrons is already comparable to that of FACET-I. Such an emittance would thus allow for a direct injection in a particle-based wakefield accelerator, without the need of a linear accelerator and emittance damp to produce the positron beam. In fact, recent studies have shown that a positron beam with degraded emittance can still be significantly accelerated using PWFA in FACET-I, at the price of achieving a lower energy gain. With respect to conventional accelerators, the emittance of the LWFA-based positrons is significantly lower than that in their initial acceleration stages. For example, the

Figure 5. Positron emittance. (a) Phase-space diagram of 1 GeV positrons exiting the converter target. (b) Energy-dependent normalised emittance of the positron at the exit of a 1-cm thick Pb target for different initial electron energies. The emittance of the positrons scales approximately as $E^{-2/3}$. 
The normalised emittance, $\epsilon$, denotes the beam energy, $E$ the average power, $Q_e$ the total charge (in a 5% bandwidth centered around 1 GeV in the LWFA case), $\sigma_x$, $\sigma_y$ the transverse sizes, $\sigma_z$ the longitudinal size, $\pi_{x,y}$ the normalised emittance, $\Delta E$ the energy spread, $f$ the frequency of operation, and $\ell$ the luminosity.

| Units          | FACET-I | FACET-II | LWFA |
|----------------|---------|----------|------|
| $E$ (GeV)      | 21      | 10       | 1    |
| $P$ (W)        | 7.4     | 9.6      | 3    |
| $Q_e$ (pC)     | 350     | 500      | 2    |
| $\sigma_x$ ($\mu$m) | 30      | 4        | 16   |
| $\sigma_y$ ($\mu$m) | 30      | 4        | 16   |
| $\sigma_z$ ($\mu$m) | 50      | 6.4      | 0.6  |
| $\pi_{x,y}$ (mm mrad) | 200     | 7        | 500  |
| $\pi_z$ (mm mrad) | 50      | 3        | 500  |
| $\Delta E$ (%) | 1.5     | 1        | 5    |
| $f$ (Hz)       | 1       | 1        | $10^{10}$ |
| $\ell$ (cm$^{-2}$ s$^{-1}$) | $5 \times 10^{25}$ | $6 \times 10^{24}$ | $10^{25-24}$ |

Table 1. Comparison with FACET-I and FACET-II the main positron beam parameters obtained in FACET-I and expected for FACET-II are compared with typical parameters at source from a laser wakefield scheme as discussed in this manuscript. The latter assumes the positron beam per bunch from a 100 pC 5 GeV primary electron beam. $E$ denotes the beam energy, $W$ the average power, $Q_e$ the total charge in the LWFA case), $\sigma_x$, $\sigma_y$ the transverse sizes, $\sigma_z$ the longitudinal size, $\pi_{x,y}$ the normalised emittance, $\Delta E$ the energy spread, $f$ the frequency of operation, and $\ell$ the luminosity.

…initial stages of SLC presented normalised emittances of 6500$\pi$ mm mrad (geometrical emittance of 500 mm mrad), and 12100$\pi$ mm mrad (geometrical emittance of 62$\pi$ mm mrad) for the case of LEP. The largely reduced emittance would allow for the injection in conventional accelerators without the need of emittance damps, that would reduce the charge in the beam and increase the cost and size of the system.

Finally, the temporal duration of the positrons by laser-driven sources is significantly shorter than the other sources. Conventional accelerators naturally produce beams with durations of the order of a few ns, which can then be treated to reduce it down to hundreds of fs, at the cost of a reduction in the charge in the bunch. The shorter duration, automatically given by the intrinsically short duration of the electron beam, presents direct advantages for applications in material science. Additionally, as mentioned earlier, the reduced longitudinal dimension of the beam is smaller than the positron-accelerating region of the wakefield in a plasma. The region of positron accelerating and focussing fields in an electron- or laser-driven plasma wakefield in the so-called bubble regime is limited to a sub-10 micron region along the propagation axis (~35 fs). Although future studies, both in particle-driven or laser-driven wakefields in FACET-II and EuPRAXIA, might open up new possibilities for a more robust and flexible positron acceleration scheme, currently only short beams fitting that region, such as the laser-driven positrons, can be efficiently accelerated by the wakefield. Furthermore, the laser-driven positrons present additional advantages. For instance, the wakefield structure can be significantly modified if a high-charge positron beam is used as a witness, reducing the peak accelerating field. Although high charges are desirable for schemes such as self-loaded PWFA, in which the positron beam both generates the wakefield and is accelerated, lower charges may be preferred in more conventional plasma wakefield accelerators to maximise the electric field and reduce the number of stages required. Finally, a laser-driven source would also present the advantage of being jitter-free, allowing a stable synchronisation on a fs-scale. This problem is partially solved by using the drive electron beam to generate the positrons by propagating through a high-Z material. However, such a procedure results in a slight worsening of the electron drive beam emittance, as well as adding the technological complication of ensuring the appropriate temporal separation between the electron drive and the positron witness beams, to ensure the synchronisation between the positron beam and the wakefield rather than the electron beam. A laser-driven source, on the other hand, would be intrinsically synchronised with a high-power laser. The lack of jittering, thanks to the laser beams being produced from the same oscillators, ensures a stable synchronisation of the different laser-driven wakefield stages, with temporal matching to the fs-level already achieved experimentally.

It should be noted, however, that in the case of TeV accelerators, beam cooling might be required in order to focus the beams to the nanometer-scale, boosting the overall luminosity. Further studies would be required regarding the cooling needs, which would come at the cost of extending the bunch longitudinal size (duration), but would allow for a broader bandwidth accepted, significantly increasing the number of positrons in the beam.

A final note must be made regarding the transport and energy selection of the laser-driven positrons. As shown earlier, the 1.00 $\pm$ 0.05 GeV positrons generated exhibit a low emittance. However, it should be noted that this energy band has to be selected from the broadband positron emission from the converter. Also, even the positrons contained in the reduced bandwidth present a significant level of divergence, rapidly expanding the beam to sizes greater than the extension of the positron-focussing fields in the wakefield, of the order of tens of microns. Therefore, the positron beam requires collimation and re-focussing in order to be further accelerated. Both collimation and energy-selection appear feasible using magnetic systems. Laser-driven schemes are compact and produce lower levels of radiation, allowing for closely-coupled experiments. Thanks to that, a compact quadrupole triplet or a plasma lens can be used to collimate the positron emission. Given the low divergence and narrow energy band considered, a large portion of the positron beam can be collected by the system, greater than 20% collected at SLC, in which a broader energy range was accepted. Once the beam has been collimated, well-known energy selection systems based on magnetic chicanes, such as those in conventional accelerators, can be implemented to select the positron energies to be further transported.
Conclusions
We have simulated the main properties of laser-driven positrons in order to test the feasibility of their injection in a multi-stage, plasma-based accelerator. From the interaction of the LWFA-driven electrons with the high-Z converter, a broadband positron beam can be generated, whose characteristics significantly improve with energy. For an electron beam similar to that proposed by the EuPRAXIA project (5 GeV, 100 pC), up to $5 \times 10^8$ positrons are generated in a energy range $1.00 \pm 0.05$ GeV, with a normalised emittance of $190 \pm 0.05$ mm mrad. Such an emittance is compatible with the further injection on secondary acceleration stages of plasma-based accelerators.

Additionally, the naturally short duration of the positron beam, similar to that of the parent electron beam, can present additional advantages towards the further acceleration in a wakefield structure, as well as being beneficial for future colliders thanks to the reduced beamstrahlung. Laser-driven positron beams can thus constitute an appealing alternative as a witness beam for beam-driven and laser-driven wakefield test facilities and, potentially, as injector of reduced cost and size for future high energy accelerators and lepton colliders.

Methods
Monte-Carlo Simulations. Simulations were performed using FLUKA (v. 2011.2.3), a nuclear physics Monte Carlo scattering code that accounts for electromagnetic cascades during the passage of an electron beam through a solid target. The numerical model for the quantum electromagnetic cascade has been extensively benchmarked and, and it is routinely checked and constantly improved to take into account any refinement in cross-section measurements in conventional accelerators. A total of $10^6$ primary electrons are simulated, propagating in a pencil-like fashion (naught divergence), from a point-source (naught source size) and emitted simultaneously. Three different cases are considered, varying the spectrum of the electrons, given by Gaussian distributions centered at 1 GeV, 5 GeV, and 20 GeV, respectively, and with an energy width of 5% of the central energy. A secondary lead converter of 1 cm thickness is placed 1 cm downstream of the electron source. In order to retrieve the parameters of interest of the generated positron beam, the Fortran routine USRBDX of FLUKA was modified. FLUKA will perform a call to the modified routine every time a condition is met by a given particle in the simulation. In the context of the results presented, the routine was executed when a positron crossed the boundaries of the converter. The phase space and time of each positron was saved upon their exit from the converter. Where applicable, the results of the simulations were normalised to the number of initial electrons, and rescaled with the 100 pC charge considered for a realistic electron beam.

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Author Contributions
The simulations were performed and analysed by A.A., the manuscript was written by A.A. and G.S., and improved through discussions with R.W. All authors reviewed the manuscript.

Additional Information
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