Magnetic field anti-symmetry of photovoltaic voltage in evanescent microwave fields

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A two dimensional electron system without spatial inversion symmetry develops a sample specific dc voltage when exposed to a microwave radiation at low temperature. We investigate this photovoltaic (PV) effect, in the case where spatial symmetry is broken by an evanescent high-frequency potential. We measure the induced PV voltage in a GaAs/Ga1-xAlxAs Hall bar at magnetic fields in the Tesla range. We find that in this regime the induced PV voltage is anti-symmetric with magnetic field, and exhibits regular Shubnikov-de Haas like oscillations. Our experimental results can be understood from a simple model, which describes the effect of stationary orbital currents caused by microwave driving.

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Coherent mesoscopic samples present remarkable rectification properties, related to the absence of spatial inversion symmetry of the disorder potential. In particular when submitted to a radio-frequency radiation they develop a dc voltage. The dependence on magnetic field of this photovoltaic (PV) effect, gives rise to random but reproducible fluctuations that were predicted theoretically [1,2] and observed experimentally in references [3,4]. In contrast with universal conductance fluctuations that obey Onsager symmetry rules [5,6], the fluctuations of the PV-voltage do not have a well defined magnetic field symmetry [7]. At high frequency this can be understood from the violation of time inversion symmetry by the microwave radiation [8,9,10]. At low frequencies, this behavior was explained through a mechanism involving electron-electron interactions [11,12,13,14,15,16]. Recently the PV effect was studied in asymmetric antidot super-lattices where magnetic field asymmetry was also present [17,18]. In all these cases however, the anti-symmetric component of the PV voltage was never larger than the symmetric one (see e.g. [19]). In this Letter we investigate the regime where the spatial symmetry of the system is broken by a non-homogeneous high frequency potential. This potential is screened in the region of the sample where the photovoltaic voltage is measured by a copper shield evaporated on the surface of the Hall bar. This reduces the mesoscopic fluctuations of the PV-voltage, revealing a PV-voltage with a dominant anti-symmetric contribution.

The system consists of two connected Hall junctions in a GaAs/Ga1-xAlxAs two dimensional electron gas (2DEG) with density n = 1.2 × 10^{11} cm^{-2} and mobility µ = 1.1 × 10^2 m^2/Vs. The sample was fabricated using wet etching and an aluminum mask. The six contacts of the Hall bar are numbered (1) – (6) (see photograph inset in Fig. 1). The four terminal resistances with source (i) and drain (j) and voltage probes k and l are defined by the usual relation R_{ij,kl} = (V_k - V_l)/I_i where V_k and V_l are the voltages on the leads (k) and (l) and I_i = -I_j is the current injected in the source lead. We measure simultaneously the Hall resistances R_{H,1} = R_{14,26}, R_{H,2} = R_{14,35}, and the longitudinal resistance R_{xx} = R_{14,23} as a function of magnetic field H. As shown on Fig. 1 our samples exhibit quantum Hall effect plateaux [21] for the Hall resistances R_{H,1}, R_{H,2} and Shubnikov-de Haas (SdH) oscillations [21] in the transverse resistance R_{xx}. We notice that the carrier density in our system is homogeneous since R_{H,1} ≃ R_{H,2}.

In the following, we excite the system with a high frequency potential V_{ac} \cos(2\pi f t) applied on a symmetrical split gate [S] shown in the inset of Fig. 1. This potential is screened by the copper top-gate deposited over

FIG. 1: (Color online) Magneto-transport properties of the Hall bar. The dashed and neighbor curves represent respectively the Hall resistances R_{H,2} = R_{14,35} and R_{H,1} = R_{14,26} (see text). The oscillating curve represents the longitudinal resistance R_{xx} = R_{14,23}. The data was acquired with a 100 nA excitation and lock-in detection at frequency 67 Hz at a temperature of 300 mK. The inset is an optical image of the sample, the leads (1) – (6) form the contacts of the Hall bar, while the electrodes [S] and [C] are local gates connected to a high frequency 50 Ω transmission line. The (orange) copper shield on top of the Hall bar can be used as a top gate to change the carrier density in the 2DEG. The black scale bar corresponds to 10 μm.
the Hall bar device and therefore the induced potential is spatially non homogeneous and vanishes exponentially inside the Hall bar \[^{22}\]. We measure the PV voltage drop \(V_{\text{pv}} = V_3 - V_2\) induced by the irradiation. In order to determine this voltage with a high precision we modulate the high frequency signal at a low frequency below 1.5 kHz. The voltage \(V_{\text{pv}}\) is then amplified by a low-noise amplifier and measured by a lock-in detector working at the frequency of the amplitude modulation. In Fig. 2, we have studied the dependence of \(V_{\text{pv}}\) on magnetic field and microwave power at fixed frequency \(f = 2.5\) GHz. The photovoltaic voltage displays oscillations as a function of magnetic field reminiscent of SdH oscillations in the longitudinal resistance \(R_{xx}\) (Fig. 2 left panel), except that the PV voltage oscillates around a zero mean value which is not the case for the longitudinal resistance. We also notice that the oscillations of \(V_{\text{pv}}\) are quenched in the quantum Hall plateau region around \(H = 2\) T (filling factor \(\nu = 2\)), in contrast to oscillations in longitudinal resistance (see Fig. 1). The amplitude of these oscillations increases with the injected microwave power \(P\). Since the microwaves are transmitted through a \(Z_0 = 50\) \(\Omega\) adapted line, \(P\) is related to the high frequency potential amplitude through \(V_{\text{ac}}^2 = \alpha Z_0 P\). Here \(\alpha\) is a frequency dependent coefficient taking into account the attenuation and reflection in the transmission line. We estimate that \(\alpha \approx 0.1\) for frequencies in the GHz range. On the right panel of Fig. 2 we show the dependence of the rectified voltage on power more quantitatively at selected values of magnetic field. We find that the photovoltaic voltage is well described by \(V_{\text{pv}} \propto P\), the deviations at higher power are attributed to heating effects. We have also performed experiments with asymmetric irradiation on the electrode \([C]\), with the electrode opposite to \([C]\) floating. These experiments lead to a similar behavior with the difference that the oscillations of the PV voltage are no longer centered around zero. For this reason we focus on the case of symmetric irradiation on the local gate \([S]\) in the rest of this article.

The Shubnikov-de Haas (SdH) oscillations of resistivity in metals and in 2DEG are symmetric with magnetic field. In contrast as illustrated on the left panel of Fig. 3, we find that the oscillations of the photovoltage are mostly anti-symmetric with magnetic field. On this figure, in order to make the connection with SdH oscillations more obvious we have shown the photovoltage \(V_{\text{pv}}\) as a function of the inverse absolute value of the magnetic field. The photovoltage displays periodic oscillations with inverse magnetic field with the exception of a missing half-period at \(H^{-1} \approx 0.5\) \(\text{T}^{-1}\) in the quantum-Hall plateau regime (filling factor \(\nu = 2\)). The right panel shows that the period of the oscillations of the photovoltage can be modified by changing the density \(n_e\) of the Hall probe with a top-gate voltage \(V_g\). This further supports the connection with SdH oscillation of resistivity whose period \(\tau_H\) is related to electron density through \(\tau_H = e/(\pi h n_e)\). We have also checked the anti-symmetry of the photovoltage at different gate voltages. The data shown on Fig. 3 was obtained for \(f = 2.5\) GHz, at lower microwave frequencies the photovoltage decreases and vanishes around \(f \approx 10\) MHz while remaining mostly anti-symmetric. We attribute this decrease to the inefficiency of our capacitive coupling at so low frequencies. We note that we are always in the regime \(2\pi f < \omega_c\) where \(\omega_c\) is the cyclotron frequency, therefore we do not expect the frequency to play an important role in contrast with recent experiments where a sharp frequency dependent PV effect was investigated around...
oscillations and zero resistance states \[24, 25, 26\]. In the plateau regions of the quantum Hall effect. The phase, which is given by the expression

\[ R \]

of induced stationary currents \(i_{dc}\) and density modulation (colored semi-disks). Frequency is \(f = 2.5 \text{ GHz}\) and \(P = 1 \text{ nW}\).

\[
\omega = \omega_c [23] \text{ in relation with microwave induced resistance oscillations and zero resistance states } [24, 25, 26].
\]

The SdH oscillations of longitudinal resistance \(R_{xx}\) as a function of inverse magnetic field have a well defined phase, which is given by the expression

\[ R_{xx}(H^{-1}) = R_0(H^{-1}) + R_1(H^{-1}) \cos\left(\frac{2\pi^2 n_c \hbar}{eH}\right) \]

where \(R_0(H^{-1})\) and \(R_1(H^{-1})\) are envelope functions weakly depending on the magnetic field on the scale of one SdH oscillation period \(\tau_H [21]\). On Fig. 4 (main figure) we compare the phase of the oscillations of \(V_{pv}\) and the phase of the oscillations in \(R_{xx}\). Our results demonstrate that the oscillation of the photovoltage are dephased by \(\pi/2\) compared to the oscillations of \(R_{xx}\). We check this by calculating numerically the integral \(\int V_{pv}(H^{-1}) dH^{-1}\) from the experimental data. We find that oscillations of this quantity are in phase with the oscillations of \(R_{xx}(H^{-1})\) (a theoretical argument justifying this comparison is given below).

In summary we find that the SdH oscillations of the PV voltage are anti-symmetric with magnetic field and are out of phase with the usual SdH oscillation of resistivity as a function of \(H^{-1}\). These oscillations are quenched in the plateau regions of the quantum Hall effect. The main lines of our explanation are the following. The high frequency potential applied on the local gate \(S\) creates a stationary current distribution \(i_{dc}\) inside the sample mostly along the y axis. A possible current distribution is shown in the inset of Fig. 4 with a simplified sample geometry. This current leads to the appearance of a static Hall voltage drop \(V_{pv} \approx R_H i_{dc}\) along the x axis perpendicular to \(i_{dc}\). For this expression to be valid, the applied potential \(V_{ac}\) must vanish in the region where \(V_{pv}\) is measured. Otherwise an additional contribution appears from mesoscopic fluctuations induced by the alternating potential. This contribution has a large symmetric component. In this respect, the evanescent potential geometry used in our experiment is crucial, and we have checked that under an homogeneous irradiation we recover an essentially symmetric photovoltage.

It is possible to derive more quantitative estimates from this heuristic scenario. The potential \(V\) on the local gate creates a modulation of the electronic density \(\delta n\) in the Hall bar. We assume that for high magnetic fields this density modulation occurs in a region of typical Larmor radius \(r_l = v_F m^*/eH\) inside the sample, where \(v_F = \hbar \sqrt{2m_e/m^*}\) is the Fermi velocity and \(m^*\) the electron mass in 2DEG (colored regions in the sketch of Fig. 4). Indeed in this regime most electronic trajectories are localized on cyclotron orbits of radius \(r_l\), which is therefore the natural length scale. The total charge induced on the Hall bar is given by \(C V\) where \(C\) is the capacitance between the local gate and the Hall bar, hence the amplitude of \(\delta n\) can be estimated as:

\[
\delta n \approx \frac{C}{r_l^2} V_{ac} \cos(2\pi ft).
\]

An approximate value of the capacitance is \(\varepsilon D\), where \(\varepsilon\) is the permittivity and \(D\) is the typical distance between the gate and the Hall bar. In the SdH regime, the amplitude of the rectified current \(i_{dc}\) is given by:

\[
i_{dc} < \frac{\partial G_{yy}}{\partial n_e} \delta n V_{ac} \cos(2\pi ft) >
\]

where < . > denotes time averaging, and \(G_{yy}\) is the conductance in y direction of the sample. Up to a geometrical factor we have \(G_{yy} \approx G_{xx}\) and in the regime where \(R_{xx} \ll R_H, G_{xx}\) is given by \(G_{xx} \approx R_{xx}/R_H^2\). As noted above, \(R_{xx} = R_0 + R_1 \cos\left(\frac{2\pi^2 n_c \hbar}{eH}\right)\) where \(R_0\) and \(R_1\) are slow functions of density and inverse magnetic field. This allows us to take into account only the oscillating term in the density derivative, which yields:

\[
i_{dc} \approx \frac{\hbar}{eH} R_1 \sin\left(\frac{2\pi^2 n_c \hbar}{eH}\right) < \delta n V_{ac} \cos(2\pi ft) >.
\]

By injecting in this formula the expression of \(\delta n\) as a function of \(V_{ac}\), and using the relation \(V_{pv} = i_{dc} R_H\) with the approximation \(R_H = H/(e n_e)\) that is accurate below 1 T, we obtain

\[
V_{pv} \approx \frac{eC}{\hbar} R_1(H) \sin\left(\frac{2\pi^2 n_c \hbar}{eH}\right) V_{ac}^2
\]

In this expression \(R_1(H)\) is the typical SdH oscillation amplitude that is symmetric with magnetic field. Consequently this expression reproduces the main features observed in our experiment: \(V_{pv}\) is anti-symmetric with magnetic field, with a phase given by \(\sin\left(\frac{2\pi^2 n_c \hbar}{eH}\right)\), and an amplitude that scales proportionally to microwave power \(V_{pv} \propto V_{ac}^2 \propto P\). This expression also leads to the right order of magnitude for the observed photovoltaic voltage, indeed for \(C \approx \varepsilon_0 D\) with \(D \approx 1 \mu\text{m}\), \(V_{ac}^2 = 1 \text{ nW} \times 50 \Omega\) and \(R_1(H) \approx 1 \text{ k}\Omega\) at \(H \approx 1 \text{T}\) we

FIG. 4: (Color online) Comparison between the behavior of \(R_{xx}(k\Omega)\) (green/grey curve), \(V_{pv}(\mu\text{V})\) (blue/black curve) and \(\int V_{pv}(H^{-1}) dH^{-1}\) (red dashed curve). The inset shows a simplified sample geometry with schematic representation (colored semi-disks). Frequency is \(f = 2.5 \text{ GHz}\) and \(P = 1 \text{ nW}\).
find that \( V_{pv} \simeq 0.1 \mu V \) (experimental amplitude is shown on the right panel of Fig. 2). Further comparison is possible by noting that the product \( R_1(H) \sin \left( \frac{2\pi n H}{\hbar} \right) \) is proportional to \( dR_{xx}(H^{-1})/dH^{-1} \). In our approximation, this leads to the simple prediction:

\[
\int V_{pv}(H^{-1})dH^{-1} \propto R_{xx}(H^{-1})
\]  

(3)

On figure Fig. 4, we show that this relation is well verified as long as \( H^{-1} \geq 1.5 \) T\(^{-1}\). Deviations are observed for higher magnetic fields, specially at \( H^{-1} \simeq 0.5 \) T\(^{-1}\) where a plateau appears in \( V_{pv} \) that is not present in \( R_{xx} \). We attribute this deviation to other quantum effects which are not taken into account in our simple model and become relevant at higher magnetic field. Specially the physics of the quantum Hall effect is important, while our model is based on a Shubnikov-de Haas approximation for conductivity. In order to confirm that the effect we have observed has a quantum origin, we have measured the temperature dependence of photovoltaic effect. Our results summarized on Fig. 5, show that the amplitude of the photovoltaic oscillations strongly decreases with temperature in the 100 mK-1 K range, in a similar way to SdH oscillations on the linear resistance.

In conclusion we have investigated the photovoltaic effect in high mobility two dimensional electron gas under irradiation by an evanescent microwave potential. We have found that the photovoltaic voltage exhibits zero centered oscillations as a function of inverse magnetic field. These oscillations are anti-symmetric with magnetic field and are out of phase with the well known Shubnikov-de Haas oscillations in resistivity as a function of inverse magnetic field. The amplitude of these oscillations is proportional to microwave power. Our experimental findings can be understood from a simple model that predicts the creation of stationary orbital currents in the sample under microwave driving. In this model the stationary voltage across the sample appears as a Hall effect detection of the orbital currents.

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[1] B.L. Altshuler and D.E. Khmel’nit’skii JETP Lett. 42, 359 (1985). A.I. Larkin and D.E. Khmel’nit’skii JETP 64, 1075 (1986).
[2] V. Fal’ko and D. Khmel’niskii, Zh. Eksp. Teor. Fiz. 95, 328–337 (1989). [Sov. Phys. JETP 68(1), 186 (1989)].
[3] R. A. Webb, S. Washburn, and C. P. Umbach, Phys. Rev. B 37 8455 (1988), P. G. N. de Vegvar, G. Timp, P. M. Mankiewich et al. Phys. Rev. B 38, 4326 (1988)
[4] A. Bykov, G. Gusev, and Z. Kvon, Pis’ ma Ekspt. Teor. Fiz. 49, 13 (1989) [JETP Lett. 49(1), 13 (1989)].
[5] S. Washburn and R. A. Webb, Adv. Phys. 35, 375 (1986)
[6] M. Büttiker, Phys. Rev. Lett. 57, 1761 (1986)
[7] D. Sanchez and M. Büttiker, Phys. Rev. Lett 93, 106802 (2004)
[8] R. Bartolo, N. Giordano, X. Huang, and G. Bernstein, Phys. Rev. B 55, 2384 (1997)
[9] DiCarlo, C.M.Marcus, and J.S.Harris, Phys. Rev. Lett.91, 246804 (2003).
[10] L. Angers, A. Chepelianski, R. Deblock, et al. Phys. Rev. B 76, 075331 (2007).
[11] J. Wei, M. Shimogawa, Z. Wang et al. Phys. Rev. Lett. 95, 256601 (2005)
[12] R. Leturcq, D. Sánchez, G. Götz et al. Phys. Rev. Lett. 96, 126801 (2006).
[13] D. M. Zumbühl, C. M. Marcus, M. P. Hanson et al. Phys. Rev. Lett. 96,206802 (2006).
[14] L. Angers, E. Zakka-Bajjani, R. Deblock et al. Phys. Rev. B 75, 115309 (2007)
[15] B.Spivak, F.Zhou and M.T. Beal Monod Phys. Rev. B 51, 13226 (1995).
[16] M. Moskalets and M. Büttiker,Phys. Rev. B 69., 205316 (2004).
[17] S. Sassine, Yu. Krupko, J.-C. Portal et al. Phys. Rev. B 78, 045431 (2008)
[18] A. D. Chepelianskiïl, M. V. Entin, L. I. Magarill and D. L. Shepelyansky, Euro. Phys. J. B 56, 1434 (2007)
[19] J-Q. Zhang, S. Vitkalov, Z. D. Kvon et al. Phys. Rev. Lett. 97, 226807 (2006)
[20] K. v. Klitzing, G. Dorda and M. Pepper, Phys. Rev. Lett. 45, 494 (1980)
[21] D. Shoenberg, Magnetic oscillations in metals, Cambridge University Press (1984) ISBN 052122480
[22] We notice that the symmetry is broken by the presence of an oval dot between the left \([S]\) and \([C]\) gates, this weak asymmetry does not play a role for the effect discussed in this article but will be analyzed more carefully in a future publication.
[23] A.A. Bykov, JETP Lett. 87, 233 (2008)
[24] M.A. Zudov, R.R. Du, J.A. Simmons, and J.R. Reno, Phys. Rev. B 64, 201311(R) (2001).
[25] R.G. Mani, J.H. Smet, K. von Klitzing et al. Nature 420, 646 (2002).
[26] M.A. Zudov, R.R. Du, L.N. Pfeiffer, and K.W. West, Phys. Rev. Lett. 90, 046807 (2003).