Quasiparticle Trapping In Three Terminal Ferromagnetic Tunneling Devices

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Abstract

Hybrid Superconductor/Ferromagnet structures have been investigated recently to address the interplay between ferromagnetism and superconductivity. They also open up new routes for the investigation of out of equilibrium superconductivity. Here, we show how it is possible for out of equilibrium excitations produced in a superconducting thin film (S) to be localized in a ferromagnetic trap (F). Specifically, a ferromagnetic nano-volume in good contact with S represents a potential well for the quasiparticles (QPs) at the gap edge. As the superconducting proximity effect is highly suppressed in F, QPs get efficiently trapped and they share their energy with the free electrons in the trap. The electronic temperature $T_e$ in the trap can be increased by up to 60% from the bath temperature at 320 mK as measured by tunneling spectroscopy using a second junction.
Superconductor/Ferromagnet (S/F) hybrid nanostructures open up new routes to study the interplay between superconductivity and ferromagnetism. The main advantage is that unlike in bulk materials, in nanostructures despite the fact that superconducting gap ($\Delta \sim \text{meV}$) and ferromagnetic exchange energy ($E_{ex} \sim \text{eV}$) are not comparable, superconductivity and ferromagnetism do not exclude one another. This is because these two antagonistic ground states influence each other only near the interface. Nonequilibrium superconductivity in such structures is a new topic. After a superconductor absorbs energy, excess quasiparticles (QPs) with non-thermal distribution are created. Their energy relaxation occurs via two different mechanisms: electron-electron ($e-e$) and electron-phonon ($e-ph$) interactions. The timescale for energy relaxation depends on the respective scattering rates ($\tau_{ee}^{-1}$ and $\tau_{e-ph}^{-1}$), both of them rapidly increasing with the excitation energy. The Fermi-Dirac energy distribution of QPs is reached on a timescale larger than $\tau_{ee}$, while in the limit of strong $e-ph$ relaxation, QP temperature becomes equal to the lattice temperature.

To be more specific, when a superconductor absorbs energy $E_0$, within a few picoseconds it goes into a nonequilibrium state, consisting of broken Cooper pairs and high energy phonons with energies close to the cutoff Debye energy. In a fast nanosecond cascade, energy is distributed over an increasing number of QPs and phonons, decaying until it reaches the gap edge. Both excess QPs and phonons have limited lifetimes. Quasiparticles may recombine into Cooper pairs, diffuse, get scattered by impurities, or get trapped and frozen, while phonons can get scattered or escape into the substrate. The characteristic timescale of QP recombination into Cooper pairs goes from the ns until a few $\mu$s depending on material parameters. If the superconductor $S_1$ is coupled to another superconductor $S_2$ via a tunnel junction, excess carriers can tunnel through the barrier. At low temperatures ($T << T_C$, where $T_C$ is the superconducting critical temperature), recombination time is longer than the tunneling time, therefore majority of QPs can tunnel, creating current through a tunnel junction. As the magnitude of current from a detector tunnel junction is inversely proportional to the volume of the source superconductor $S_1$, in order to enhance the readout signal, Booth proposed the idea of QP trapping in a small volume layer that can be either a superconductor with a smaller gap than that of $S_1$ or a normal metal. We show a typical quasiparticle trapping device on Fig.1. The current is injected into the device via
a tunnel junction from superconductor $S_{inj}$, and detected through another tunnel junction with superconducting electrode $S_2$.

We have considered a ferromagnetic trap ($F_{tr}$) and investigated the energy confinement produced by downconversion of QPs coming from $S_1$ into $F_{tr}$. As no gap is induced in $F_{tr}$ by proximity effect, a ferromagnetic trap allows QPs to relax their energy in a volume much smaller than that of a normal trap, increasing the QP accumulation and hence the local energy density. We have fabricated three terminal Josephson tunnel devices of different sizes and geometries. QPs are injected into $S_1$ from a tunnel junction, they relax at the gap edge and then they are trapped in $F_{tr}$ where through $e$-$e$ interaction they locally raise the electron temperature $T_e$. The temperature of these nonequilibrium carriers in $F_{tr}$ is probed by tunneling spectroscopy, measuring the current-voltage characteristics of a second tunnel junction connecting $F_{tr}$ layer and $S_2$. We show that in mesoscopic devices, ferromagnetic trapping is efficient in raising the local electronic temperature from the bath temperature of 320 mK up to 580 mK.

The paper is organized as follows. In section II, we describe the principle of quasiparticle trapping. In section III we present the principle of operation of three terminal tunnel junction devices using a ferromagnetic trapping layer. In section IV we describe our three terminal macroscopic device consisting of two stacked tunnel junctions and present its characterization in terms of conductance variation with QP injection. In section V we present our planar mesoscopic three terminal device, consisting of two tunnel junctions connected with a sub-micrometric S/F bilayer. We also measure conductance as a function of steady-state current injection. In section VI we discuss the results and trap heating in terms of a simple non-equilibrium model.

II. PRINCIPLE OF QUASIPARTICLE TRAPPING

As first proposed by Booth, trapping of excitations in a small junction has been considered as an alternative to fabrication of large area detectors, whose high capacitance limits both the frequency response and the energy resolution. Excess QPs created by either Cooper pair breaking or injection (see Fig.1) diffuse from $S_1$ to the trap, where they relax their energy and are confined. From this intuitive physical picture, it is clear that the trap layer has two crucial functions: it prevents back diffusion of QPs, and with its smaller volume it increases
the magnitude of the readout signal, since the density of out of equilibrium quasiparticles \( N_{QP} \), for a fixed energy, is proportional to the inverse of the trap volume \( N_{QP} = I_{inj}\tau_{tr}/eV_{tr} \), where \( I_{inj} \) is the injected current, \( V_{tr} \) the trap volume and \( \tau_{tr} \) the time spent in the trap before relaxation. However, if the volume is too small, phase coherence is preserved in the trap resulting in a superconducting proximity effect. The induced gap in the density of states in the trap reduces the number of QPs available to relax the energy, and hence heating.

The choice of materials for the Superconductor/Trap (\( S_1/T \)) bilayer is, therefore, crucial for correct operation. Firstly, \( S_1 \) will be chosen for long QP lifetimes and high QP diffusion velocities to ensure that QPs reach the trap before recombination. Secondly, it is important that interfaces between \( S_1 \) and \( T \) are clean, to facilitate the diffusion. Thirdly and most importantly, we need a small superconducting proximity effect in the trap layer. We should make a trap layer sufficiently thin in order to get a high density of nonequilibrium QPs, but not too thin as it should remain in the normal state in contact with \( S_1 \) through a highly transparent interface. Despite considerable efforts in several laboratories, the right compromise between these constraints is still under investigation.

N.E. Booth et al.\(^7\) and Ullom et al.\(^8,9\) have extensively studied normal trap efficiency, defined as the ratio between detected and injected power, in a system consisting of an Al superconducting reservoir \( S_1 \), and Ag as the normal metal trap. They used a three terminal device following the diagram shown in Fig.1. Tunneling through a detector junction determines the dwell time and the speed of the detector, both of the order of \( \mu s \). Ullom et al. described the QP diffusion in terms of a renormalized, energy dependent diffusion coefficient \( D_E = (v(E)/v_F)D \), where \( v(E) = v_F[1 - (\Delta/E)^2]^{1/2} \) is the QP group velocity that drops to zero at the gap edge, \( \Delta \) is the superconducting gap, \( v_F \) the Fermi velocity, \( E \) the energy measured from the Fermi level and \( D \) is the bulk diffusion coefficient. They have measured at 100 mK up to 17% efficiency. Because of the large device size (\( \sim 100 \mu m \)), QP losses were mainly due to recombination. In another series of experiments with excitations produced in In crystals by a low power pulsed laser, Goldie et al.\(^5\) studied trapping into Al and Cu thin films (250 to 500 nm) deposited on In always finding a minigap induced in the Cu by the proximity effect. Pepe et al.\(^10\) reported nonequilibrium measurements under steady state current injection in a stacked double superconducting tunnel junction device with middle electrode consisting of an Nb/Al bilayer where the Nb is the superconductor and the Al the trap. They found that the 20 nm thick Al trap layer was strongly proximised by a 40
nm thick Nb film. They also found that the proximity effect is reduced as a function of the injection current, without any appreciable modification of the interface transparency. Zehnder has studied how external energy is stored for different junction materials. He found losses mainly due to the presence of the sub-gap phonons in the trapping layer. Efficiency scales inversely with the mean free path of the material. He also pointed out that for large area (50 × 50 µm²) Nb/Al structures the density of states is spatially dependent. As a consequence, the trapping process becomes local, and hence both QP lifetime and trapping rate.

In the present work we propose a new direction, the reduction of the trap volume using a ferromagnet \( F_{tr} \). The superconducting proximity effect extends in the ferromagnet over a coherence length given by \( \xi_F = (\hbar D/E_{ex})^{\frac{1}{2}} \) that varies between 0.1 and 10 nm and is almost 100 times smaller than the coherence length of a normal metal with the same diffusion constant, \( D \). This extremely reduced proximity effect provides a more efficient energy localization. So, a hybrid, mesoscopic S/F heterostructure seems to be a unique candidate to obtain the smallest, not proximised trap.

III. THREE TERMINAL DEVICE OPERATION

Here we describe the working principle of our realization of the ferromagnetic quasiparticle trapping transistor (FQTT) based on the description proposed by Booth et al. The ferromagnet is a Pd_{0.9}Ni_{0.1} alloy. We choose this alloy because: 1. the small ferromagnetic coherence length (\( \sim 10 \) nm); 2. Pd has an almost filled \( d \) band, and the large density of states at the Fermi level provides more conduction electrons available in the trap; 3. electronic specific heat is high (\( \sim 3 \) orders of magnitude higher than pure Copper, for example), which means that energy is "stored" in the electron gas, with substantially longer \( e-ph \) relaxation time. It is worthwhile to point out that long \( e-ph \) relaxation time leads to a small bandwidth.

The principle of operation of our devices can be obtained considering a simple static balance of power flow into the \( F_{tr} \) layer. To do this, we borrow the common semiconductor transistor terminology. We call \( S_1/F_{tr} \) bilayer the base, \( S_{inj} \) the emitter, and \( S_2 \) the collector. Current \( I_{inj} \) is passed through the first junction emitting \( I_{inj}/e \) quasiparticles. The net power injected into \( S_1 \) is \( P_{inj} = (I_{inj}/e) \varepsilon_{inj} \), where \( \varepsilon_{inj} \) is the average injected QP energy, which depends
on the voltage $V$ across the tunnel junction. A part of the incoming power is lost via thermal interaction with the phonon lattice, $P_{th}$. It can be calculated using the so-called 2-T nonequilibrium model,\textsuperscript{16} in which different temperatures $T_e$ and $T_{ph}$ and specific heats $C_e$ and $C_{ph}$ are assigned to the electron and phonon systems, which are considered to be decoupled at low temperatures. The energy transfer rate from electrons to phonons in the $S_1/F_{tr}$ bilayer is given by $P_{th} = \Sigma V_{tr} (T_e^5 - T_{ph}^5)$, where $\Sigma$ is a material-related parameter (varying in the range of 1-5 nW/µm$^{-3}$K$^{-5}$) and $V_{tr}$ is the volume of the trap. Here we explicitly assume that the phonon system is at the external bath temperature. This hypothesis, as we shall see later, depends on the details of the film geometry and coupling to the substrate, via the Kapitza interface conductance.\textsuperscript{17} Injected power is also evacuated via the detector tunnel junction, by cooling through tunneling. This happens when a NIS junction is biased at a voltage $V$ lower than the superconducting gap, so that only the hot electrons from the tail of the Fermi distribution can tunnel from the normal to the superconducting electrode. Self cooling, by removing high energy electrons, causes a progressive transfer of energy out of the normal film.\textsuperscript{18} The cooling power of the junction when polarized at the gap edge is given by $P_{cool} \approx (0.5 \Delta_2^2 / e^2 R_T) (k_B T / \Delta_2)^{3/2}$,\textsuperscript{19} where $R_T$ is the normal state resistance of the junction. In the experiments described below the cooling power can be neglected and hence as we shall see below all the injected energy is lost by phonon interactions:

\[(I_{inj}/e) \varepsilon_{inj} - \Sigma V_{tr} (T_e^5 - T_{ph}^5) \approx 0,\]

which yields:

\[T_e = T_{ph} \left[ 1 + \frac{(I_{inj}/e) \varepsilon_{inj}}{\Sigma V_{tr} T_{ph}^5} \right]^{\frac{1}{5}}. \tag{1}\]

If high energy QPs are injected with $\varepsilon_{inj} \gg \Delta_1$, the most efficient mechanism for energy redistribution within the electron subsystem becomes the emission of Debye phonons. The mean free path of these phonons is very small, and they efficiently excite additional electrons and break Cooper pairs in the $S_1$ reservoir. Nonequilibrium vibrations isotropically propagate through the whole system, mixing and coupling the electronic and phononic subsystems. As a result, delocalized heating takes place and energy confinement is no longer possible. Therefore it is important to work at energies near the gap edge in order to avoid phonon losses (which multiply with the increase of the injection energy) and transfer the injected energy solely to the electronic system.
IV. STACK JUNCTION DEVICE

We have fabricated two kinds of three terminal structures with different geometries and sizes. In both we chose Al as superconductor $S_1$ for its long recombination time. The first macroscopic device that we shall present consists of two stacked junctions (area of $0.7 \times 0.7 \text{mm}^2$). We put electric contacts so that we can bias each junction independently. The stacked structures used for the experiment described in the following are sketched in Fig. 2 in a top (a) and cross-section (b) view. Four stacked junctions are fabricated simultaneously on a single Si wafer, with common bottom electrode. All layers were fabricated in situ using thin film evaporation, in an ultra high vacuum system with a base pressure of $10^{-9}$ mbar. The fabrication procedure is as follows. On a Si substrate we evaporated through a metallic mask the first 50 nm-thick Al layer. This layer will be the bottom electrode $S_2$ of the device, common to all the junctions of the sample. Then we oxidize the Al layer by O$_2$ plasma at about $8 \times 10^{-2}$ mbar pressure. The junction area is defined by evaporating 50 nm-thick orthogonal striplines of SiO in order to define a square of $0.7 \times 0.7 \text{mm}^2$. Then, a layer of PdNi (10% Ni) is evaporated as ferromagnetic trap $F_{tr}$. We have varied the thickness (5, 8, 10 nm) of the Pd$_{0.9}$Ni$_{0.1}$ (PdNi) layer. The trap volume is $V_{tr} = 2500 \mu \text{m}^3$ for 5 nm of PdNi. Then we evaporated 250 nm of Al as superconducting layer $S_1$. We repeated the oxidation and SiO deposition in order to make a second tunnel barrier, and finally evaporated 50 nm of Al as layer $S_{inj}$.

The junctions quality was systematically checked by measuring the current-voltage characteristics and the tunnel conductance with the standard ac modulation technique. All the measurements were carried out at 320 mK in a $^3\text{He}$ cryostat. In Fig. 2(c) and (d) are shown two typical I-V curves and tunnel conductance spectra of an Al/Al$_2$O$_3$/Al (SIS) junction and an Al/Al$_2$O$_3$/PdNi-Al (SIF) junction, respectively. Quasiparticle current is suppressed below $360 \mu \text{V}$, i.e. twice the Al gap for the upper SIS junction, while for the bottom SIF junction we measure a voltage gap of $195 \mu \text{V}$ showing no proximity effect in F. The tunneling spectrum of the bottom junction is well fitted by the conventional BCS density of states (dashed line), instead the upper junction shows that the Al on the PdNi has not fully recovered its BCS density of states and states in the gap are partially occupied. Normal resistances are $140 \Omega$ for SIS and $4 \Omega$ for SIF junction. The critical temperature of the PdNi/Al bilayer is $1.2 \text{K}$. 
We measured the dynamical conductances of the bottom junction under injection of current between 0 and 600 µA from the top junction. We did not observe any enhancement in the detection spectra at energies close to the gap, while at energies 50 or even 100 times larger, zero bias conductance increases linearly in power (variations of about 10% of the normal state conductance are measured) due to hot electrons. We have also reversed the roles of the junctions. The injected power is of the order of µW in both configurations. As shown in Fig. 3, marker groups (1) and (2) refer to the injection and detection in the same stack. Markers (1) corresponds to injection from the SIF and detection at the SIS and markers (2) to the inverse. As \( E > \Delta \), phonon emission drives the relaxation process, we measure twice higher signal when injecting from the SIF (1) rather than the SIS (2) junction because of the double convolution by the QP density of states of the two superconducting electrodes.

Markers (3) refer to injection and detection between junctions of different stacks. All marker groups (3) are practically superimposed, regardless of the direction of injection. No differences are observed in the detector as a function of the distance from the injector. Therefore even though energy is not localized in \( F_{tr} \), the lack of accumulation is not due to the out diffusion of the QPs away from the detector junction area into the surroundings. Indeed, from the recombination time \( \tau_r = 100 \mu s \) which sets the upper limit for QP diffusion, we found diffusion length \( L_r \approx 10 \mu m \), which is small compared to the dimensions of our device. Moreover, we did not register any difference between the injection from the top/bottom junction of the stack and detection with the bottom junction of the neighboring stack. This implies, as the bottom electrode is geometrically common to all the junctions of the sample, that the tiny raise in the tunneling conductance (i.e. markers (3)) is mainly due to a small rise in the substrate temperature (we also did not measure any thermal gradient between neighboring junctions). Let us consider the power balance and the dynamics of excitations in the PdNi trap. We calculate specific heat of electron and phonon subsystems: \( C(\text{mJ/molK}) = \gamma T + \beta T^3 \), where the linear contribution is due to electrons and cubic to phonons. From the molar volume of the trap (8.64 cm³/mol) we have: \( \gamma_M = 1.38 \cdot 10^{-15} \text{J} \mu \text{m}^{-3} \text{K}^{-2} \) and \( \beta_M = 1.7 \cdot 10^{-17} \text{J} \mu \text{m}^{-3} \text{K}^{-4} \) and hence: \( C_e = 1.0 \cdot 10^{-12} \text{J/K} \) while \( C_{ph} = 1.2 \cdot 10^{-15} \text{J/K} \) at 300 mK. We found that the electron-phonon conductance \( (dP_{ph}/dT_e \equiv G_{e-ph} = 5\Sigma(Ad)T_e^4) \) at \( T_e = 300 \text{ mK} \) is 0.2 µW/K and the electron-phonon scattering time \( (\tau_{e-ph} = C_e/G_{e-ph}) \) is 5.1 µs. Once thermal excitation is transferred to the lattice, energy can flow by thermal conductance to the substrate. This transfer is limited by thermal boundary resistance,
the Kapitza resistance, $R_K$. Typically, $R_K T^3 = 5 \cdot 10^{-4} \text{K}^4 \mu\text{m}^2\text{W}^{-1}$. Thus the effective conductance will be:

$$G_K = \frac{\text{Area}}{R_K} = \frac{T^3}{5 \times 10^{-4} \left[\text{Area}/\text{m}^2\right]} \text{W/K}.$$ 

There are two boundaries to consider: PdNi to Al bottom electrode, and bottom electrode to substrate. We neglect the boundary between the surface oxide on the substrate and the single crystal Si wafer. So, taking as area a larger value of about $1 \text{mm}^2$ and considering the series of two interfaces, we obtain $G_K = 27 \mu\text{W}/\text{K}$, which implies $G_K$ about a factor 100 larger than $G_{e-ph}$. The phonon temperature is uniform on the sample. This implies that our substrate has very good coupling to the $S_1/F_{tr}$ bilayer.

We now discuss why the ferromagnetic trap is not working properly. The trap works at the gap edge and, in our case, at that energy the flow of injected QPs is too small. In fact, the density of out of equilibrium QPs in the trap must be higher than that in the thermal equilibrium, $N_{QP} > N_{0,QP}$, for the trap to be effective. This condition imposes a lower bound on the lifetime of the out of equilibrium excitations in the trap $\tau_{tr}$ as $N_{QP} = I_{inj}\tau_{tr}/eV_{tr}$ and $N_{0,QP} = n(\varepsilon_f)k_B T$, where $I_{inj}$ is the injected current (typically of about $1 \mu\text{A}$ at the gap edge with our resistance values), $V_{tr}$ is the trap volume, and $n(\varepsilon_f)$ is the density of electron states at the Fermi level. We estimated that $\tau_{tr}$ of about $300 \mu\text{s}$ is required to accumulate excitations with a number higher than $N_{0,QP}$. This time is much larger than any characteristic timescale and in particular $\tau_{e-ph}$, thus excitations out of equilibrium created by injection are practically lost via phonons. The trap is inefficient and the conductance at zero bias independent of injection at energy comparable with the Al gap edge.

The first obvious solution is to increase the injected current density.

V. MESOSCOPIC PLANAR DEVICE

We fabricate a new type of mesoscopic planar device to get smaller volumes and higher trap efficiency. This type of device is represented in the photo of Fig. 4(b). Two sub-micrometric tunnel junctions are separated by middle, double layered Al-PdNi common electrode, the trap.

The fabrication is as follows. We used a trilayer suspended mask consisting of 600 nm of polymer polyether sulphone (PES), 60 nm Si$_3$N$_4$ layer, and 400 nm PMMA layer. The mask is patterned by electron beam lithography and the pattern transferred to the Si$_3$N$_4$ layer.
by SF$_6$ plasma reactive ion etching at a pressure of 10 mbar for about 60 seconds. Then
the PES is etched with O$_2$ plasma at a pressure of 300 mbar for 10 minutes, which gives an
undercut of about 500 nm. The SEM photo of the mask is shown on Fig. 4(a). Our samples
were fabricated by angle evaporation in an ultrahigh vacuum system with a base pressure
of about $10^{-9}$ mbar. First 50 nm of Al were evaporated. The Al was oxidized in pure O$_2$ flux
at a pressure of $5 \times 10^{-2}$ mbar. Then a 50 nm-thick Al layer was evaporated, followed by
a 5 nm-thick PdNi layer. Four devices are fabricated on the same wafer. The schematic of
the device is shown in Fig. 4(c). The first, right-side $300 \times 500 \text{nm}^2$ Al/Al$_2$O$_3$/Al junction
is separated by another junction of the same area by a 4 $\mu$m long Al layer which is partially
($\sim 3 \mu$m) recovered by a thinner ferromagnetic PdNi layer. The magnetic layer is used to
suppress superconductivity by inverse proximity effect and it defines the trap. Trap volume
is $V_{tr} = 0.15 \mu m^3$ i.e. about 100 times smaller than the trap used in the stacks.
Note that the F layer plays a slightly different role in this device, since the QPs coming
from the Al superconducting electrode tunnel into the Al and then diffuse lateraly into the
PdNi/Al bilayer made up of the same Al. As the reservoir and the trap are made of the
same material, matching of the Fermi velocities is optimal and so is the QP transmission.
Furthermore, in this planar structure we deal with lateral trapping, which allows to avoid
back tunneling of QPs, responsible for reduced cooling power.$^{21}$
In Fig. 5 the I-V curves of the Al/Al$_2$O$_3$/Al (SIS) and the Al/Al$_2$O$_3$/Al/PdNi (SI/SF)
junctions are shown. The normal state resistances are about 750 $\Omega$ and 500 $\Omega$ respectively.
Junction resistances higher than those measured in the stacks result in reduced injected
power (now ranging from 50 pW to 1 nW). The gap voltages are 400 $\mu$V and 200 $\mu$V, as
expected for inverse proximity effect. Moreover, the I-V curve of the SI/SF junction is well
fitted by integrating the BCS density of states with an Al energy gap of 190 $\mu$eV and a base
temperature of 320 mK (see Fig. 6). The SIS junction is hysteretic with critical current
of 200 nA and retrapping current of 85 nA. The finite resistance at zero bias is due to the
bilayer trap resistance in series with the junction. The principle of the experiment is the
same as that described above. Out of equilibrium excitations are collected in the SF trap
rising the electron temperature $T_e$, which is measured by tunneling spectroscopy. Different
conductance spectra were measured while increasing the DC injection current through the
SIS junction from 0.3 to 8 $\mu$A, as shown in Fig. 6. We obtain $T_e$ from the BCS fits also
shown in Fig. 6 as red curves. The electron temperature $T_e$ as a function of the injected
power
current is plotted in Fig. 7, top panel, markers. The temperature rises rapidly up to 0.53 K, and then reaches 0.98 K more slowly, resulting in two different slopes. Unlike stack junctions, the temperature in the planar trap increases significantly for the injection of QPs with energy comparable with the superconducting gap energy. Furthermore, the crossover between these two regimes is set by a voltage bias corresponding to the gap edge as expected because trapping, and hence energy localization, are more efficient below the gap edge. As injection energy increases (∼ 40 times more for $I_{\text{inj}} = 8 \mu A$), out of equilibrium phonons are emitted before the QPs reach the trap. High energy relaxation occurs mainly by phonons and phonon losses reduce the energy localized in the trap, resulting in a smaller temperature increase.

VI. TRAP HEATING

For $E < \Delta_{\text{inj}}$ quasiparticle energy relaxation in the trap is possible because, firstly, at 0.3 K the trap size is larger than $L_{ee} = (D\tau_{ee})^{1/2} = 3 \mu m$, secondly, the electron-phonon scattering time is much longer than $\tau_{ee} \sim 10 \text{ ns}$ and thirdly, the trap is located at a distance of about a micrometer from the SIS junction. This distance is much smaller than the recombination length $L_r \sim 100 \mu m$ as estimated above. An estimation of the electron-phonon scattering time from the electron-phonon conductance $G_{e-\text{ph}} = 1.6 \text{ pW/K}$ and the specific heat $C_e = 6 \times 10^{-15} \text{ J/K}$ gives $\tau_{e-\text{ph}} = 0.5 \mu s$. The effective surface trap area evaluated from the SEM image is about $3 \mu m^2$ and it gives $G_K = 160 \text{ pW/K}$ Kapitza conductance from the phonon bath to the substrate. As $G_K >> G_{e-\text{ph}}$, the phonons in the device are thermalized at the phonon base temperature. The bandwidth of the device is limited by the smallest between thermal tunneling and electron-phonon time. In Table I are summarized all the relevant physical parameters that determine QP trapping, for both stacks and mesoscopic devices investigated here.

In Fig. 7 (top panel, full line) we report the temperature increase as estimated from Eq. (1) considering negligible cooling by tunneling. (An estimate gives about 2 pW, a factor hundred smaller than the injected power.) The actual temperature increase is lower than that obtained considering only cooling by phonons (solid line). Instead, we found good agreement by introducing a QP thermal loss (dotted-dashed line), $\kappa \Delta T$, where $\kappa$ is the thermal conductivity of the Al leads whose normal state resistance is $1.2 \Omega$. 

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Now let us discuss the current gain. The excess current of the SI/FS junction normalized to the value for zero injected current, $\Delta I_C/I(0)$, for three different voltage bias values, is shown in Fig. 7 bottom panel. When biasing well above the gap voltage (curve C on Fig. 7 corresponding to point C on Fig. 5, $V_C = 0.28\,\text{mV}$), no excess current is measured. This range corresponds to the high energy tails of the QP DOS and it is almost independent of injection. When we approach the gap voltage we measure more pronounced variations of the collected current. When we polarize the detector junction at $V_C = 0.1\,\text{mV}$ (i.e. below the gap voltage, point A on Fig. 6) we measure an increase of the tunnel current up to 15 times. As expected, it is at energies near the gap that the increase of current is maximum: at $V_C = 0.18\,\text{mV}$, point B on Fig. 6, the collected current is up to 35 times $I_C(0)$. It is important to note that the trapping mechanism not only controls the number of out of equilibrium QPs, but also the direction of the energy flow.

If we reverse the roles of the junctions, injecting from the SI/SF and detecting at the SIS, we do not register any increase of output current. All the current values detected in the reversed configuration fall below the dashed line in Fig. 7 low panel. Therefore, the ferromagnetic trap introduces a strong asymmetry in the device. Good isolation is very interesting for applications. However the amplification parameter as defined by Booth, $\beta = I_C/I_{inj}$, where $I_C$ and $I_{inj}$ are, respectively, the collected and injected currents, normalized to the current gap values $I_{C0} = I_{inj0} = \Delta_A/\rho_N$, is 0.24 for detection at constant normalized voltage $V_C = 0.8$. Higher amplification may be achieved at lower temperature and highly thermally isolated traps.

**VII. CONCLUSION**

We have investigated a three terminal device consisting of two superconducting tunnel junctions coupled via an S/F bilayer. The ferromagnetic layer is used to localize and multiply QPs injected from the base junction. QP excess current is measured through the second detecting tunnel junction. We measured conductance spectra of the detecting junction as a function of the injected power for two types of structures fabricated with the same S/F materials: a stacked macroscopic and a planar mesoscopic device. We have found efficient trapping in the mesoscopic device, where it is possible to increase the local electronic temperature by up to 60% of the base temperature. We have also found that input is well
TABLE I: The physical parameters which determine the QP dynamics in both traps are summarized. First column refers to the stacked macroscopic devices, and the second to the planar mesoscopic structures.

| Device                       | Macroscopic stacked | Mesoscopic planar |
|------------------------------|---------------------|-------------------|
| Trap volume [cm$^3$]         | $10^{-9}$           | $10^{-13}$        |
| $G_{e-ph}$ [nW/K]            | 200                 | 0.02              |
| $\tau_{e-ph}$ [$\mu$s]      | 5                   | 0.5               |
| $G_C$ [nW/K]                 | 2.2                 | 0.01              |
| $\tau_t$ [$\mu$s]           | 700                 | 0.07              |
| Injected power [nW]          | 1000                | 1                 |

isolated from the output as a consequence of using the ferromagnetic trap, making the device attractive for transistor-like operation. However the gain at 320 mK is 0.24.

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FIG. 1: (Color online) Principle of quasiparticle trapping. Quasiparticles coming from the superconducting reservoir $S_1$ with the energy comparable to the gap fall into the potential well $F_{tr}$, and interact with the electrons, heating them. A tunnel barrier $I$ in direct contact with the trap electrode allows the readout of the nonequilibrium current signal. The measurement principle is also shown. We are able to bias the two junctions in different configurations.
FIG. 2: Sketch of the top view (a) and the cross-section (b) of the stacked device. The junction area is $0.7 \times 0.7 \text{mm}^2$ and the distance between junctions on the same sample is about 1 mm. Experimental I-V curves (black) and conductance spectra (red curves) of the top (c) SIS and bottom (d) SISF junction of the stacked device. Normal resistances are, respectively, $140 \Omega$ and $4 \Omega$. (d) the BCS fit (dashed line) of the conductance spectrum at $T = 0.32 \text{ K}$ and gap value of $0.195 \text{ meV}$ is also shown.
FIG. 3: Tunneling conductance variation at zero bias (normalized to the normal state conductance) as a function of the injected power. Marker groups (1) and (2) refer to the injection and detection in the same stack. Markers (1) corresponds to the injection from the SIF and detection at the SIS and markers (2) vice versa. Markers (3) refer to the injection and detection between junctions of different stacks.
FIG. 4: (a) SEM image of the trilayer mask. (b) SEM image of the planar device. The Al/Al₂O₃/Al (SIS) junction on the right and Al/Al₂O₃/Al/PdNi (SISF) junction on the left are shown in the inset. They are connected by a 1 µm wide Al/PdNi bilayer. (c) The schematics of the device. DC currents are injected from the right SIS and detected through the SISF junction.
FIG. 5: I-V curves of the Al/Al₂O₃/Al (SIS) junction (red) and the Al/Al₂O₃/Al/PdNi (SISF) junction (blue). The SIS junction shows a Josephson critical current of 200 nA and a retrapping current of 85 nA.
FIG. 6: Experimental I-V curves (dots) and BCS fits (red lines) of the detector junction under a DC current injection between 0.3\textmu A and 8\textmu A.
FIG. 7: (Top panel) Electronic temperature in the trap, as a function of the injected current. Markers refer to the electronic temperature extracted by the experimental conductance spectra via a BCS fit. The change in the slope occurs approximately at 0.7 µA, corresponding to the Al gap. The full line represents the expected increased temperature, calculated from the electron-phonon coupling. The dotted-dashed line corresponds to the increase of the electronic temperature due to the Al QP thermal conductivity. (Bottom panel) Extra-current (i.e. the difference between the detected current with and without injection, normalized to the respective value without injection: $\Delta I_C/I_C(0)$) at three different polarization values (A, B, C points are given in Fig. 5), as a function of the injected current.