Constraints on Lorentz Invariance Violation with Fermi-LAT Observations of Gamma-Ray Bursts

C. Couturier\(^1\), V. Vasileiou\(^2\), A. Jacholkowska\(^1\), F. Piron\(^2\), J. Bolmont\(^1\), J. Granot\(^3\), F. W. Stecker\(^4\), J. Cohen-Tanugi\(^5\), F. Longo\(^5\)

1 LPNHE, Université Pierre et Marie Curie Paris 6, Université Denis Diderot Paris 7, CNRS/IN2P3
2 LUPM, Université Montpellier 2, CNRS/IN2P3
3 Department of Natural Sciences, The Open University of Israel
4 Astrophysics Science Division, NASA/Goddard Space Flight Center and Department of Physics and Astronomy, University of California
5 Istituto Nazionale di Fisica Nucleare, Sezione di Trieste and Dipartimento di Fisica, Università di Trieste

camille.couturier@lpnhe.in2p3.fr

Abstract: Arrival times of photons from four bright GRBs observed by Fermi-LAT have been analyzed in order to detect a possible Lorentz Invariance Violation (LIV), related to a non trivial dispersion of light in vacuum. No delays have been detected and strong limits on the Quantum Gravity (QG) energy scale are derived: for linear dispersion we set tight constraints placing the QG energy scale above the Planck mass; a quadratic leading LIV effect is also constrained.

Keywords: Fermi, gamma-ray bursters, Lorentz invariance, Quantum gravity, vacuum dispersion

1 Introduction/Motivation

Several Quantum Gravity (QG) theories allow for a violation of the Lorentz invariance (LIV), that can manifest as a dependence of the velocity of light in vacuum on its frequency (see [1][2] for examples of such models). These QG effects causing LIV are supposed to arise at a specific energy scale, namely $E_{\text{QG}}$, believed to be of the order of the Planck energy ($E_{\text{Planck}} \simeq 1.22 \times 10^{19}$ GeV). If such a dependence exists, then photons of different energies emitted together by a distant source will arrive on Earth at different times. Amelino-Camelia et al. [3] have parametrized the possible LIV time delays using a series expansion of powers of the photon energy over $E_{\text{QG}}$. Specifically, the degree of dispersion due to LIV effects $\tau_n$ — defined for two photons as the ratio of their delay in arrival $\Delta t$ over the difference of their energies (resp. of their squared energies) $\Delta(E)$ — is connected to $E_{\text{QG}}$, to the distance of the source $H_0$, and to the Hubble constant $H_0$, $n = 1$ (resp. $n = 2$) accounting for linear (quadratic) LIV effects:

$$\tau_n = \frac{\Delta t}{\Delta(E^n)} \simeq s_k \frac{(1+n)}{2E_{\text{QG}}^nH_0} \kappa_n$$  \hspace{1cm} (1)

with

$$\kappa_n = \int_0^\infty \frac{(1+z)^{n} dz'}{\sqrt{\Omega_m(1+z)^3 + \Omega_{\Lambda}}}$$  \hspace{1cm} (2)

and $s_k = -1$ (resp. +1) in superluminal (subluminal) case, i.e. if the photons are faster with larger (smaller) energies. The cosmological parameters are fixed here to those derived from WMAP results [4]: $\Omega_m = 0.24 \pm 0.02$, $\Omega_{\Lambda} = 0.73 \pm 0.03$, $H_0 = 70.4 \pm 1.4$ km.s$^{-1}$.Mpc$^{-1}$.

A direct consequence of equation (1) is that any measurement (or limits) on the dispersion parameter $\tau_n$ with photons detected in a well-located (i.e. with known redshift) gamma-ray source can lead to a measurement (or limits) on the energy scale $E_{\text{QG}}$.

The full analysis and results have been already published [5], here we give an overview.

| GRB     | Redshift | $k_1$  | $k_2$  |
|---------|----------|--------|--------|
| 080916C | 4.35 ± 0.15 | 4.44   | 13.50  |
| 090510  | 0.903 ± 0.003 | 1.03   | 1.50   |
| 090902B | 1.822 ± 0.001 | 2.07   | 3.96   |
| 090926A | 2.1071 ± 0.0001 | 2.37   | 4.85   |

Table 1: Distances of analyzed GRBs.

2 Data

High-energy (GeV) transient emissions from distant astrophysical sources such as Gamma-ray Bursts (GRBs) and Active Galaxy Nuclei can be used to search for and constrain LIV. The Fermi LAT and GBM collaborations have previously analyzed two GRBs in order to put such constraints. In this analysis, four bright Fermi-LAT GRBs are used; their distances are given in table 1. For GRB090510, the time and energy profiles are given in figure 1.

Selection The event selection P7_TRANSIENT_V6 is a less restrictive selection of LAT events optimized for signal-limited analyses such as this one. We analyzed photons with energies above 30 MeV. To minimize systematic errors due to GRB spectral evolution (a well known property of GRB emissions), the time intervals were chosen to focus on the main peaks of emission. Other method-specific cuts are discussed in the next section.

3 Data analysis: methods

Three methods, complementary in terms of sensitivity and probing different aspects of the lightcurves, have been used: PairView (PV), Sharpness Maximization Method (SMM) and Maximum likelihood (ML). Configuration details for each method are given in table 2.

3.1 PairView

This new method has been developed for this study; the principle is to calculate the following ratios between all the pairs of photons $(i, j)$ with $i \neq j$:

$$L_{i,j}(n) = \frac{t_i - t_j}{E_{i}^{n} - E_{j}^{n}}$$  \hspace{1cm} (3)
Table 2: Configuration details. $\rho$ is the tuning parameter used in the SMM’s sharpness measure; $N_{100}$, the number of events above 100 MeV used with PV and SMM; $\gamma$, the photon index of the spectrum of detected events assuming the energy distribution follows a power-law ($\propto E^{-\gamma}$). $E_{\text{cut}}$ is the separating energy between the $N_{\text{template}}$, low-energy events used for building the lightcurve template and the $N_{\text{fit}}$, high-energy events used in the calculation of the likelihood.

| GRB     | Time Range (s) | $\rho$ | $N_{100}$ | $\gamma$ | $N_{\text{template}}$ | $N_{\text{fit}}$ | $E_{\text{cut}}$ (MeV) |
|---------|----------------|-------|-----------|----------|-----------------------|------------------|------------------------|
| 080916C | 3.53–7.89      | 50    | 59        | 2.2      | 82                    | 59               | 100                    |
| 090926B | 5.79–14.21     | 80    | 111       | 1.9      | 57                    | 87               | 87                     |
| 090510  | 0.01–3.11      | 50    | 157       | 1.5      | 148                   | 118              | 125                    |
| 090926A | 8.92–10.77     | 25    | 60        | 2.2      | 53                    | 48               | 47                     |

where $\rho$ is a parameter defined a priori for each GRB from simulated datasets so as to maximize the sensitivity of the method. Small (resp. large) values of $\rho$ will result in the method focusing on small (large) timescales.

3.3 Maximum likelihood
A model of the emission of photons at the source is built and then used to calculate the probability that the events in the data characterized by $(t_i, E_i)$ have been subject to dispersion by a factor $\tau_i E^{\gamma}$.

Several assumptions/simplifications have been made:
- the energies are well reconstructed (no smearing);
- the energy distribution follows a power-law spectrum of index $\gamma$ (cf. table 2);
- no spectral variability (e.g. variation of index $\gamma$ with time) shows up;
- the emission lightcurve (at the source) is approximated by the lightcurve of the lowest-energy events (in the data).

These assumptions lead to the following probability density function (PDF) of emission:

$$ P(t_i, E_i | \tau) = \frac{1}{N_{\text{pred}}(E)} \Lambda(E) f(t_i - \tau_i E^{\gamma}) $$

where $N_{\text{pred}}(E)$ is the number of photons emitted by the source, $\Lambda(E)$ the observed power-law spectrum, $f$ a parametrization of the emission lightcurve, obtained from a 2- or 3-gaussian fit of the low energy event times.

A separating energy $E_{\text{cut}}$ is chosen so as to split the dataset into two sets: the $N_{\text{template}}$ lowest-energy events (with $E < E_{\text{cut}}$) are used to build a template lightcurve, while the $N_{\text{fit}}$ highest-energy events ($E > E_{\text{cut}}$) are processed in the calculation of the likelihood.

4 Data analysis: confidence intervals
The measurement of the dispersion $\tau$ (directly in the data) doesn’t distinguish between dispersion arising from LIV effect itself (we call it $\tau_{\text{LIV}}$) and spectral variability as the source, that could mimic a dispersion factor ($\tau_{\text{sm}}$). Hence we have

$$ \tau = \tau_{\text{LIV}} + \tau_{\text{sm}} $$

(6)

Previous studies have ignored the term $\tau_{\text{sm}}$, assuming $\tau = \tau_{\text{LIV}}$. Here, we calculate a first confidence interval (CI) on the total degree of dispersion $\tau$: we then give a CI for the dispersion possibly arising because of LIV effects $\tau_{\text{LIV}}$ based on conservative assumptions on $\tau_{\text{sm}}$.

4.1 Confidence intervals on $\tau$.

The CI is done in different ways for PV/SMM and ML.

For PV and SMM, sets are created by randomizing the associations of time and energy from the original dataset.
By definition, the time and energy distributions will remain the same; yet the mixing of times and energies is expected to remove any possible dispersion in the data. A hundred thousand of these sets are produced, the PV or SMM method is applied to get the best estimate $\hat{\tau}_n$ of the dispersion parameter $\tau_n$ for each set. The resulting distribution, $f_n$, is used to approximate the PDF of the measurement error on $\tau_n$ (general case of any $\tau_n$): $\epsilon = \hat{\tau}_n - \tau_n$. We then calculate a CI for $\tau_n$ from the quantiles of $f_n$.

For ML, calibrated CIs were calculated using Monte Carlo simulated sets. These sets have the same statistics, lightcurve model and spectrum as the original data. No intrinsic dispersion was artificially added. Each simulated data set produces a lower limit and an upper limit on $\tau_n$ from cuts on the likelihood profile. The calibrated lower (resp. upper) limit of the CI is taken as the mean of the distribution of the per-set individual lower (upper) limits.

4.2 Confidence intervals on $\tau_{\text{LIV}}$

No reliable model of GRB emission at LAT energies ($E > 100$ MeV) has been produced yet, therefore a conservative estimation of the impact of $\tau_{\text{int}}$ is taken as chosen. We assume that the measurements of $\tau_n$ are dominated by GRB intrinsic effects, so the PDF of $\tau_{\text{int}}$ is to match the dispersion allowed by the data: $\langle \tau_{\text{int}} \rangle = 0$, since all the measures on $\tau_n$ don’t exclude a trivial dispersion; and the width has to match the width of $\tau_n$. Since the intrinsic effect is set to perfectly match any observed dispersion, the CIs on $\tau_{\text{LIV}}$ are built so that they have the largest possible width. The way the PDF $P_{\text{int}}(\tau_{\text{int}})$ is implemented depends on the method.

For PV and SMM, the PDF of the measurement error on $\epsilon' = \zeta_n - \tau_{\text{LIV}}$ is built as the autocorrelation of $\tau_n$ from cuts on the likelihood profile. The calibrated lower (resp. upper) limit of the CI is taken as the mean of the distribution of the per-set individual lower (upper) limits.

5 Results

Total degree of dispersion $\tau_n$ Figures 2 demonstrate the application of the PV, SMM and ML methods on GRB090510 for the linear case ($n=1$).

The measurements of $\tau_n$ parameter for each method, for both linear and quadratic cases, are summarized in Table 3. The limits obtained on the four bursts with the three different methods are compatible with no dispersion. The likelihood method gives the more stringent constraints.

LIV-induced dispersion $\tau_{\text{LIV}}$ New CIs on the LIV-induced dispersion parameter $\tau_{\text{LIV}}$ have been produced, as explained in section 4. We don’t provide here their values for each GRB; limits on EOG using these specific CIs have been produced (see below).

Table 3: Measurements of the total degree of dispersion $\tau_n$ for each method. Limits are for a 99% double-sided confidence level.

| GRB Name | PairView | SMM | Likelihood |
|----------|----------|-----|------------|
|          | (Lower Limit, Best Value, Upper Limit) | (Lower Limit, Best Value, Upper Limit) | (Lower Limit, Best Value, Upper Limit) |
|          | (s GeV$^{-1}$) | (s GeV$^{-1}$) | (s GeV$^{-1}$) |
| GRB090510 (10$^5$) | -0.46 -0.06 0.88 | -0.6 -0.12 1 | -0.6 -0.12 1 |
| GRB090510B | -0.56 -0.18 0.18 | -0.66 -0.20 0.23 | -0.56 -0.18 0.18 |
| GRB090526A | -0.32 -0.10 0.23 | -0.45 -0.17 0.15 | -0.52 -0.18 0.18 |
| GRB090510 (10$^6$) | -0.18 -0.05 0.012 | -0.12 -0.06 0.012 | -0.44 -0.06 0.14 |
| GRB090510B | -0.32 -0.06 0.012 | -0.12 -0.06 0.012 | -0.44 -0.06 0.14 |

Table 3: Measurements of the total degree of dispersion $\tau_n$ for each method. Limits are for a 99% double-sided confidence level.

6 Systematic uncertainties

GRB-intrinsic effects Previous analyses of Fermi GRB data have shown that the emission falls into different spectral components: a Band component at MeV energies, and a power-law component at higher energies. The difference in time emission between the two components could be misidentified as a LIV effect. The cuts ($E > 100$ MeV) used for PV and SMM limit the contribution of Band-originated events. The cuts at a lower energy ($E > 30$ MeV) used for the ML method makes it possibly more sensitive to this effect. However, a dedicated analysis of the data didn’t show any sign of time lag between the two spectral components.

Also, spectral evolution has been detected in many Fermi-LAT GRBs and can be misinterpreted as LIV effect. Focusing on the time windows with higher variability (namely the peaks of the lightcurve) allow to reduce the influence of this effect in present analysis.

Instrument The energy reconstruction uncertainty due to high off-axis angles is negligible. Difference between true and reconstructed energies leads to systematics of $\sim 10\%$ ($n=1$) and $\sim 15\%$ ($n=2$). For the ML method, the dependence of the effective area on the energy has been neglected: this systematic uncertainty is dominated by statistical uncertainty on the spectrum.

Other effects Background contamination is negligible (very low rate). Uncertainty on the redshift is $\sim 1\%$ (GRB080916C) and $\sim 0.1\%$ (other). The uncertainty on the cosmological parameters is $\sim 3\%$.

1. the value of the cut is set so as to get exact coverage.
Figure 2: Application of the PV, SMM and ML methods on GRB090510 for the linear case (n = 1).

Figure 3: 95% one-sided CL limits on $E_{\text{OG}}$ for subluminal (s = +1, left) and superluminal (s = -1, right) cases, for a linear (n = 1, top) and quadratic (n = 2, bottom) LIV effect. Each triplet of points corresponds to one GRB and shows, left to right, the limits obtained with PV, SMM and ML (from $\tau_n$). The horizontal bars correspond to an averaged over the three methods limit for the intrinsic-corrected case (from $\tau_{\text{LIV}}$).

7 Conclusions

The analysis of the four GRBs did not lead to the observation of a significant energy dependence of the speed of light in vacuum. However, it was possible to place robust limits on the $E_{\text{OG}}$ scale. The best limits were obtained for the shortest GRB (GRB90510), which is also the closest one: for the linear/subluminal case, $E_{\text{OG},1} > 7.6E_{\text{Planck}}$ using the total degree of dispersion $\tau_n$ and $E_{\text{OG},1} \gtrsim 2E_{\text{Planck}}$ using the LIV-induced degree of dispersion $\tau_{\text{LIV}}$ (limits at 95% CL). Observing short GRBs at high redshift would possibly improve this limit. A discussion of the systematics, including taking into account possible source effects, has also been conducted. Detailed analysis and discussion can be found in [5].

References
[1] Mattingly, Living Rev.Rel. 8 (2005)
[2] Jacobson et al., Annals Phys. 321 (2006) 150-196
[3] Amelino-Camelia et al., Nature 393 (1998) 763-765
[4] Komatsu et al., Astrophys.J.Suppl. 192 (2011) 18
[5] Vasileiou et al., Phys. Rev. D 87 (2013) 122001 arXiv:1305.3463
[6] Cranmer, Comp. Phys. Com. 1363 (2001) 198-207
[7] Band et al., Astrophys.J. 413 (1993) 281-292
[8] Scargle et al., Astrophys.J. 673 (2008) 972
[9] Abdo et al., Nature 462 (2009) 331
[10] Abramowski et al., Astropart. Phys. 34 (2011) 738

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