A Novel Metaheuristic Optimization for Throughput Maximization in Energy Harvesting Cognitive Radio Network

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Abstract—In this article, a novel technique is proposed, namely rank-based multi-objective antlion optimization (RMOALO), and applied to optimize the performance of the energy harvesting cognitive radio network (EHCRN). The original selection method in multi-objective antlion optimizer (MOALO) is suitably changed to improve the algorithm, thus reaching the optimal solution for the problem. The proposed technique shows considerable performance improvement over the method used in the multi-objective antlion optimizer (MOALO). The performance of the proposed RMOALO is demonstrated on five benchmark mathematical functions and compared to multi-objective particle swarm optimization (MOPSO), multi-objective moth flame optimization (MOMFO), MOALO-Tournament, and MOALO-Roulette. The simulation results show an improved convergence of RMOALO and find the optimal solution to the throughput maximization problem. We show that RMOALO provides 16.33% improved average throughput with the optimal value of sensing duration for the varying amount of harvested energy compared to MOPSO, MOMFO, MOALO-Roulette, and MOALO-Tournament.

Index Terms—Cognitive radio; Energy harvesting; Metaheuristic optimization; MOALO; Spectrum sensing.

I. INTRODUCTION

The demand and popularity of efficient wireless networks have increased over the past decade. Cognitive radio (CR) has been shown to be an emerging technology in wireless networks [1]. Cognitive radios are battery-operated with a limited network lifetime [2], [3]. With the advent of new devices, the efficient use of spectrum and energy has become a concern for most researchers. Energy harvesting is a promising addition to cognitive radio networks (CRN) to save energy and maximize throughput in next-generation wireless networks [4]. Energy harvesting is achieved from different energy sources in an energy harvesting cognitive radio network (EHCRN). The sources of energy in [5] are ambient such as solar, wind, motion, etc. from where the energy is harvested. The cognitive radio system uses ambient energy sources in [6], [7]. The RF (radio frequency) signal utilized by the secondary network acts as a source depending on the state of the channel in [8].

To meet the aforementioned challenges, optimization of the parameters that affect the performance of the energy harvesting cognitive radio network is considered [9]. To efficiently utilize the energy harvesting from the primary transmitter (PT), both energy harvesting and information transfer can be accomplished using the separated spectrum sensing and energy harvesting scheme (SSSEH). It can improve wireless network throughput, sensing time, and reduce the risk of collision between the primary transmitter and the primary receiver.

II. RELATED WORKS

For the EHCNRN in [10], the average throughput of the secondary network is maximized by an optimal pairing of the sensing duration and the energy detector sensing threshold. In [11], a hidden Markov model describes the imperfect spectrum sensing process. The network obtains the optimal solution while adapting its parameters based on quality of service (QoS) requirements [12]. Some previous works have maximized throughput by optimizing resource allocation between primary and secondary users [13]. To maximize the throughput of the secondary user, optimal spectrum sensing energy, the transmit energy, and spectrum sensing interval Markov decision process (MDP) framework is used in [14]. In [15], optimized sensing time is achieved to improve the throughput in CR with a trade-off between the two. The optimization problem solved in [16] with the energy constraint and the collision constraint maximizes the total throughput of the secondary network in which the ambient source has been used for harvesting. Optimization of sensing threshold and sensing duration jointly for throughput maximization of a CRN is studied in [17]. The throughput of CRN is maximized by maintaining a proper trade-off between the harvested energy and the transmission of data with an optimal transmission time for primary and secondary users in [18]. In [19], the harvesting interval and the transmission interval are optimized to maximize the total achievable throughput of cognitive radio networks to obtain the maximum total achievable throughput. The sensing interval problem of the idle and busy channels in the EHBased CR network was formulated in [20]. A Markov chain was developed to find the energy state transition probability to solve the energy wastage problem.

From the literature, it is seen that spectrum sensing
optimization has been extensively studied, and most of the researchers emphasized optimizing the trade-off for spectrum sensing and throughput in EHCRN by solving it as a convex optimization problem [18]–[20].

Despite the advances mentioned above, there is still a trade-off between throughput and sensing in EHCRN with constraints on interference and energy [21]. For example, the CR needs to sense the spectrum with the minimum energy in less time to get overall maximum throughput. These problems are solved using classical optimization techniques. These existing optimization methods incorporate high complexity if the problem has a trade-off and multiple parameters to be handled simultaneously. Constrained optimization problems are more challenging to solve than unconstrained optimization. Such constraints and trade-offs can be dealt with using metaheuristic-based multi-objective optimization, as it provides an optimal solution by optimizing two or more objectives simultaneously. Moreover, these techniques offer faster convergence and provide global solutions efficiently. Although in the literature [22], the issues of efficient resource utilization are solved using dynamic programming or mixed-integer nonlinear programming (MNLP) but with a high computational cost.

For cognitive radio network (CRN), up to the authors knowledge, metaheuristic-based multi-objective optimization methods have been used in related topics in [23]–[25] and have given satisfactory results, but we are not sure about separated spectrum sensing and energy harvesting scenario (SSSEH) in energy harvesting cognitive radio networks where energy harvesting and spectrum sensing occur separately in particular. Motivated by the works mentioned above, the focus of our work is to improve the performance of an energy harvesting cognitive radio network with the maximum throughput requirement while satisfying energy and interference constraints. This is achieved by multi-objective optimization of the EHCRN using the proposed novel metaheuristic technique. Constrained optimization can be a great solution to existing spectrum and energy problems. Analytical expressions for throughput and energy ratio are developed under the separated spectrum sensing and energy harvesting (SSSEH) scenario. The performance comparison of throughput under parameters similar to the baseline technique proposed in [26] is made. The impact of interference, signal-to-noise ratio (SNR), and harvested energy on throughput is also studied.

We have implemented the optimization problem of throughput maximization using multi-objective particle swarm optimization (MOPSO) [27], multi-objective moth flame optimization (MOMFO) [28], multi-objective antlion optimization (MOALO)-Roulette and MAOLO-Tournament [29] in the separated spectrum sensing and energy harvesting (SSSEH) scenario. These optimization techniques lack the proper trade-off between their intensification and diversification processes and get stuck to the best local solution.

Thus, we propose a rank-based multi-objective antlion optimization algorithm (RMOALO), which can prevent the solution from getting stuck in the local optimum to find the global optimal sensing time, maximizing the average throughput. Additionally, RMOALO is tested for various benchmark functions to validate its effectiveness. Apart from this, the performance comparison of the proposed algorithm with other metaheuristic algorithms shows that RMOALO outperforms in reaching the optimal solution. The comparison helps to find the best suitable algorithm for the given problem. The key contributions of this research work are summarized as follows:

1. Formulation of throughput maximization as a non-convex optimization problem using the novel fitness function for average throughput in separated spectrum sensing and energy harvesting (SSSEH) scenario.
2. An improved rank-based multi-objective metaheuristic optimization algorithm is proposed and used to find an efficient global solution. The benchmarking of the proposed algorithm with the state-of-the-art metaheuristic algorithms is also done.
3. The simulated results compared with the conventional scheme demonstrate that the proposed metaheuristic algorithm substantially increases the throughput of the secondary transmitter (ST).

The rest of the paper is organized as follows. Section III introduces the system model of the separated spectrum sensing and energy harvesting scheme (SSSEH) in EHCRN. For the network’s maximum throughput demand, the multi-objective optimization problem for throughput maximization is formulated in Section IV. A novel multi-objective algorithm is proposed to obtain the optimal sensing duration in Section V. Section VI presents the simulated results and discussions. Section VII concludes the paper and presents future work.

III. SYSTEM MODEL

The system model of CR equipped with wireless energy harvesting for separated spectrum sensing and energy harvesting (SSSEH) is illustrated in Fig. 1.

![Fig. 1. Energy harvesting cognitive radio system for separated energy harvesting and spectrum sensing.](image)

It consists of a primary and secondary network. The primary network consists of the primary transmitter-receiver pair and the secondary network consists of a secondary transmitter-receiver pair. The secondary transmitter (ST) is equipped with an RF energy harvester consisting of a rectifier unit and a rechargeable battery. The ST uses harvest-store-use for guaranteed QoS [30]. The primary network uses a licensed spectrum and has a fixed power source. Primary transmitter and receiver use synchronous slotted communication with the duration of the slot “T”. The
secondary network is not licensed to use the spectrum, but opportunistically accesses the licensed user’s spectrum depending upon the availability of the primary user. The ST senses the spectrum periodically according to the spectrum state of \( (H_0 \text{ or } H_1) \) to harvest energy, signal sensing, and data transmission. \( H_0 \) gives the primary receiver state as an idle spectrum state and \( H_1 \) as an occupied spectrum state. The frame structure of SSSEH is illustrated using Fig. 2 [31].

1. Energy harvesting: In the interval \((0, T_1)\), if the primary transmitter is present, the energy harvester at the ST harvests from the RF signal of PT. The energy harvested is stored in the battery for future use. If the primary transmitter is absent, the energy harvester at ST stops as no RF signal will be present. In the absence of PT, harvesting is not done. The secondary transmitter is OFF during this time interval, i.e., there is no transmission in this phase. The ST works in the next phase using the stored energy, as there will be no RF energy due to the absence of PT.

2. Spectrum sensing: In the time slot \((T_1, T_2)\), the energy harvester at the secondary transmitter stops harvesting and senses the spectrum. Spectrum sensing is performed with the energy of the storage device.

3. Data transmission: In the time slot \((T - T_2, T)\), if the primary user is not detected, the sensing stops, and the data transmission occurs using the stored energy. During the data transmission slot, it becomes crucial to avoid collisions due to traffic between the primary transmitter-receiver pair. So, the energy and collision constraints are considered.

### TABLE I. PRINCIPAL SYMBOLS’ GLOSSARY.

| Symbol | Meaning |
|--------|---------|
| \( \tau_1 \) | Energy harvesting time |
| \( \tau_2 \) | Sensing duration |
| \( \sigma_n^2 \) | Noise Variance |
| \( \sigma^2_s \) | Signal Variance |
| \( T \) | Total frame period |
| \( P_{in} \) | Probability of signal transmission without collision |
| \( P_i \) | Probability of signal transmission with collision |
| \( S(m) \) | Primary transmitter signal |
| \( W(m) \) | Noise signal |
| \( R_i \) | Average throughput at secondary |
| \( P_n \) | Energy arrival Rate |
| \( P_e \) | Target Collision probability |
| \( E_s \) | Average energy harvested at harvester |
| \( E_s^2 \) | Average energy at secondary |
| \( P_s \) | Energy consumed for sensing by secondary transmitter |
| \( P_i \) | Sensing probability |
| \( e_i \) | Energy required for data transmission |
| \( E_n \) | Energy consumed for transmission at the secondary transmitter |
| \( E_n^2 \) | Upper Bound |
| \( v_i \) | Number of iterations |
| \( \theta_n \) | Channel status \( n \)th position |
| \( \phi_i \) | Fitness value of the ant \( i \)th position |
| \( C_i \) | The minimum value of variables for the ant at \( i \)th position |
| \( P_f \) | False alarm (probability) |
| \( P_d \) | Detection (probability) |

![Fig. 2. The frame structure of separated energy harvesting and spectrum sensing.](image)

### IV. PROBLEM FORMULATION FOR MULTI-OBJECTIVE OPTIMIZATION

This section aims to formulate a fitness function for throughput maximization and the energy ratio at the secondary transmitter (ST).

#### A. Energy Harvesting and Consumption

The energy harvester in the secondary transmitter harvests energy from the RF signal of the primary transmitter if there is no user signal. As shown in Fig. 2, each frame duration is \( "T" \) and the energy arrival is random, with \( P_n \) as the average rate. In the harvesting slot, the average harvested energy is given as \( E_h = P_{ST} \), which is available to the ST in the sensing slot. The secondary transmitter executes spectrum sensing operation using energy detection and consuming energy \( E_s = e_i \tau_2 \) in the sensing phase, where \( e_i \) is the power required for spectrum sensing. The assumption made in this model is that the energy harvested in different harvesting time slots is not dependent on the channel between the primary transmitter and the RF energy harvester.

The Markov process is used to model the state occupation of the channel [32]. The sensing results of the channel being occupied or idle are given by the channel occupation state as \( \theta_n \in \{0 \text{ (idle), 1 (occupied)} \}\) for the slot \( n \). The state transition probabilities with the channel occupancy state are illustrated in Fig. 3.

![Fig. 3. State transition diagram.](image)

Here, the probability of transit is \( q_i \) for the idle state and \( q_o \) for the occupied state. Thus, the steady-state probabilities are given by \( \pi_i = \frac{1-q_o}{2-q_i-q_o} \) and \( \pi_o = \frac{1-q_i}{2-q_i-q_o} \), respectively [17], with \( \pi_i + \pi_o = 1 \).

Let \( e_i \) represent the power required for data transmission. If the secondary transmitter finds the spectrum occupied, i.e., \( \theta_n = 1 \), it starts harvesting the energy from the primary transmitter but does not consume energy for data transmission. If the channel is idle, i.e., \( \theta_n = 0 \), the secondary transmitter consumes \( E_s = e_i(T - \tau_1 - \tau_2) \) (1 - \( \theta_n \)) energy during the transmission phase. Thus, the expression for the average energy consumed in slot \( n \) at ST is
The probability of no collision while sensing when the primary channel used by the primary network is idle. The throughput of the secondary network when the primary network is idle is 

\[ P_s = \log(1 + \gamma_s), \]

where \( \gamma_s \) is signal-to-noise ratio at the input of the secondary transmitter

\[ P_s = P_s(\tau_s, \varepsilon, P_b)(1 - P_c(\tau_s, \varepsilon)), \]

where \( P_s(\tau_s, \varepsilon, P_b) \) is the probability of the secondary transmitter being active. The system is considered active from a long-term perception. There is an upper bound on the activation probability in SSSEH given by

\[ P_s(\tau_s, \varepsilon, P_b) = \min(1, Est(\tau_s, \varepsilon, P_b)). \]

**Case II Primary network is occupied.** Let \( P_c(\tau_s, \varepsilon, P_b) \) denote the probability of collision while sensing when the primary channel is occupied. The throughput of the secondary network when the channel is occupied is

\[ R_s = \log(1 + \frac{\gamma_s}{1 + \gamma_s}). \]

The received signal-to-noise ratio in the secondary network for secondary and primary signals is \( \gamma_d \) and \( \gamma_h \), respectively

\[ P_s(\tau_s, \varepsilon, P_b) = P_s(\tau_s, \varepsilon, P_b)(1 - P_c(\tau_s, \varepsilon)). \]

The average throughput of the ST depends on the probability that the secondary transmitter transmits without collision and in the presence of collision. Thus, the normalized average throughput \( R_s \) using (6) and (7) is given as

\[ R_s = \min(1, Est(\tau_s, \varepsilon, P_b)). \]

Protection of the licensed user, i.e., the primary receiver, is of utmost importance. So, when the channel of the primary network is occupied, the collision probability should be less than its target value

\[ P_c(\tau_s, \varepsilon, P_b) \leq P_n, \]

where \( P_n \) is the target collision probability of protecting the primary network. Here, the sensing duration is a crucial term to which throughput maximization is achieved. Therefore, the novel fitness function used for sensing duration optimization is formulated as

\[ \max_{\tau_s} R_s(\tau_s, \varepsilon, P_b), \]

subject to \( P_c(\tau_s, \varepsilon, P_b) \leq P_n, E_s \leq E_h. \)

To maximize the fitness function in (11), the rank-based multi-objective optimization (RMOALO) is proposed to optimize the sensing duration and solve the problem of throughput maximization in the given optimization problem.
V. PROPOSED META-HEURISTIC ALGORITHM (RMOALO) AND OTHER TECHNIQUES TO SOLVE SENSING DURATION OPTIMIZATION PROBLEM IN SSSEH

We use multi-objective optimization algorithms to solve the constrained optimization problem with multiple variables. In particular, MOPSO, MOMFO, MOALO, and the proposed RMOALO are used to solve duration optimization problem for the sensing. A brief description of these algorithms is given below.

A. Multi-Objective Particle Swarm Optimization

MOPSO [27] extends particle swarm optimization (PSO) to handle multiple objectives. Multi-objective particle swarm optimization incorporates Pareto dominance into PSO. This concept creates preferences among the swarm particles, developing leaders and guiding other particles. These different leaders are the solutions, but only one leader is selected to update the velocity that represents their movement.

MOPSO involves the basic steps:
- Initialization of the population of particles “i” as pop[i] and the velocity of each particle vel[i]. Each particle “i” has a position pop[i] ∈ rep, representing a possible solution. After a certain time, the position of the particle is obtained by adding its velocity, vel[i] ∈ rep, to pop[i]
  \[ \text{pop}[i] = \text{pop}[i] + \text{vel}[i]. \] (12)
- Evaluate each of the particles in the population and store the position of the particles in the population representing non-dominated solutions and leaders in the repository (rep).
- Initialize the memory of each particle that guides it to travel through the search space. This memory is also stored in the repository.
- The velocity of a particle “i” is based on the best position already fetched by the particle, pbest[i], and the best position already fetched by the set of neighbors of “i”, rep, which is a leader of the repository
  \[ \text{vel}[i] = I W \times \text{vel}[i] + r_1 \times (\text{pbest}[i] - \text{pop}[i]) + r_2 \times \times(\text{rep}[h] - \text{pop}[i]). \] (13)

The coefficient I W is the particle inertia that controls how much the previous velocity affects the current one and takes a value of 0.4; r 1 and r 2 are random numbers in the range [0...1]. If the new position and the current pbest[i] are non-dominated, the new value is chosen randomly between these two vectors. rep[h] is a particle from the repository, chosen as a guide for i.

As there are many best solutions from which the fittest one should be chosen, but due to lack of exploitation, MOPSO is incapable of searching globally. Therefore, it converges early without finding the fittest solution. Hence, we tend to solve the problem with the MOMFO algorithm.

B. Multi-Objective Moth Flame Optimization

MOMFO has modified Moth flame optimization [33] that includes the following steps.
- Initialize the position of “i” number of “m” moths and “j” number of “f” flames.
- For each moth position, evaluate fitness.
- Store the non-dominated solutions in the repository, i.e., positions of the moth.
- Find the best local position for each moth in the first iteration, update the moth position in the second iteration onwards, and compare the updated position of moth with the previous position.
- The position of each moth “i” is updated with respect to jth flame
  \[ m_i = S(m_i, f_j), \] (14)

where S designates a spiral function which permits each moth to fly around a flame; it is not clear that the moth has to fly in the space between the moth position and the flame. It can also discover the other space. Therefore, there is a more efficient exploration and exploitation of the search space by moths
  \[ S(m_i, f_j) = d \times e^t \cos 2\pi t + f_j, \] (15)

where d is the absolute distance |f j - m i|, b is the constant for controlling the shape of the logarithmic spiral function, t is a random number between [-1, 1]. Furthermore, the reduction in number of flames N f is adaptive and is reduced with respect to the increase in iteration
  \[ N_f = \text{round}\left( N_{f_{\text{max}}} \frac{N_{f_{\text{max}}}}{I_{\text{maxiter}}} \right), \] (16)

where N f max is the maximum number of flames. The MOMFO has the capability to reach the best solution due to efficient exploration and exploitation of the search space as this algorithm updates the position based upon the absolute distance between moth and flame.

C. Multi-Objective Antlion Optimizer (MOALO)

MOALO is the extended version of Antlion Optimization (ALO) and follows the same search behavior as ALO. It is inspired by the unique hunting behavior of antlions. Antlions are net-winged insects, and the chosen prey are ants. Antlions form the cone-shaped trap in the sand for ants while throwing out the sand [34].

Mathematical Modeling of MOALO. The mathematical modeling of hunting includes five different steps: search agents with random walk, trap formation, trap ants, catching prey, trap reconstruction, and elitism [35].

Random walk of search agents. The search for food makes the ants move stochastically over the search space. The hunting process of antlions is modeled by the interaction of the antlions with the ants modeled by random walk as
  \[ X(t) = \{0, \text{cumsum}(2r(t_j) - 1), \text{cumsum}(2r(t_j) - 1)\} \] (17)

The cumulative sum is calculated by cumsum with the maximum number of iterations as max-iter and r(t) as a stochastic function, and t indicates the random walk step, and the rand is any number between 0 and 1
The steps of the ant should be within defined boundaries, so
\[ X'_i = (X'_i - a_i) \times (d'_i - C'_i) \div (b_i - a_i) + C'_i, \]
where \( a_i \) and \( b_i \) signify the \( i \)-th ant variable showing the minimum and maximum random walk. For each iteration, \( C'_i \) and \( d'_i \) represent the \( i \)-th variable indicating the minimum and maximum at the iteration \( t \), respectively.

**Trap ants.** The random walk of ants is affected by the hypersphere traps represented by vectors \( c \) and \( d \) set by the Antlions:
\[ c'_i = \text{Antlion}_j + c', \]
\[ d'_i = \text{Antlion}_j + d', \]
where \( c' \) and \( d' \) are the minimum and maximum of all the variables in the \( t \)-th iteration, \( \text{Antlion}_j \) at the \( t \)-th iteration represents the position of the selected \( j \)-th antlion.

**Sliding ants towards antlions.** The ants slid towards antlions by shooting the sand outwards by them. The trapped ants slide down, thus preventing them from escaping. Hence, reducing the boundaries of the random walk of the ant to get a decreasing radius of the hyperspheres is modeled as:
\[ c' = \frac{c'}{I}, \]
\[ d' = \frac{d'}{I}, \]
where \( I \) is a ratio for controlling the radius, \( c' \) and \( d' \) is the minimum and maximum of all the variables at the \( t \)-th iteration.

The ratio \( I = 1 + 10^{-w_1 T} \), where \( T \) represents the current iteration, \( T \) is the maximum number of iterations, and \( w \) is defined based on the current iteration.

**Catching prey and reconstruction of the pit.** The prey caught (ant) at the bottom of the pit becomes fitter than its corresponding antlion. An antlion is then required to update its position to the latest position of the hunted ant to catch new prey in the next iterations. The following equation simulates this
\[ \text{Antlion}_j = \text{Ant}_i \text{ if } f(\text{Ant}_i) < f(\text{Antlion}_j). \]

Here, \( t \) denotes the current iteration and \( \text{Ant}_i \) specifies the \( i \)-th position of the ant at iteration \( t \). The function \( f \) denotes the fitness value, and \( < \) shows the \( \text{Ant}_i \) rules \( \text{Antlion}_j \).

**Elitism.** Maintaining and saving the fittest antlion obtained at any point of the optimization process depends on the concentration of solutions in the search space and is known as elitism. The elite antlion is the fittest antlion in each iteration
\[ \text{Ant}_i = \frac{R'_i + R''_i}{2}, \]
where \( R'_i \) is the random walk around the antlion in iteration \( t \), and \( R''_i \) is the random walk around the elite in iteration \( t \).

The archive is updated with the solutions explored in the next iteration. The selected solution is based on the probability using the equation as follows
\[ P = \frac{c}{N_i}, \]
where \( N_i \) represents the number of solutions for the \( i \)-th solution in the neighborhood, and \( c \) is a constant with a value greater than 1.

As MOALO gives diverse new solutions having very close values, it is necessary to handle this behavior with a suitable algorithm.

**D. Proposed Novel Rank-based Multi-Objective Antlion Optimization (MOALO)**

The strength of a metaheuristic algorithm on a given optimization problem is determined by its ability to provide a balance between the global search and the local search. The proposed algorithm (see Algorithm 1) uses rank-based selection instead of the roulette wheel selection used in MOALO. To prove the competence of this selection method, we have also implemented MOALO with a tournament-based selection method. Tournament selection is used in one of the variants of antlion optimization (ALO) [36]. MOALO uses a repository to store non-dominated Pareto optimal solutions obtained at a given point in time. Solutions are then chosen from this repository using a roulette wheel mechanism based on the coverage of solutions as antlions to guide ants towards promising regions of multi-objective search spaces. The selection probability of all individuals becomes almost identical, which works against the basic idea of genetic algorithms. Thus, we proposed the algorithm, which is named a “rank-based multi-objective optimization algorithm” (RMOALO). Rank-based selection involves sorting all the random walks in decreasing order, arranging them in a queue, and moving towards the ants from the higher-order rank to the lower one. Therefore, the position of ants in (25) updated using a roulette wheel is modified to rank selection, helping to faster convergence. Thus, the arrangement of random walk of ants is listed in decreasing order and ranked accordingly followed by the rank of ants:
\[ p_1^i \geq p_2^i \geq p_3^i \ldots \ldots \ldots p_n^i, \]
Algorithm 1. Pseudocode of the RMOALO algorithm.

1. Initialize ant (potential solutions) of normalized sensing period \( x \in (0,1) \) with population size \( N \), and max number of iterations.
2. Assign the value for parameters \( T \), \( E_r \), \( E_s \), \( N \) (for which algorithm needs to be executed).
3. Calculate Fitness value, i.e., Average Throughput function for each solution from step 1. Fittest
4. Select Antlion using Rank. Update its respective position (elite antlion).
5. While (iteration count is less than max iteration)
   for (Each antlion)
   Antlion to be selected by rank selection method.
   Randomly walking ants are slided in to the trap as per following criteria: opt=Rand:
   if opt > 0.75
   lb=Antlion+ub;
   elseif opt > 0.5
   lb=Antlion-ub;
   elseif opt > 0.25
   lb=Antlion+lb;
   else
   lb=Antlion-lb;
   ub=Antlion-ub;
   end
   Generate random walk of Ant’s path around elite antlion
   Generate random walk of Ant’s path around the shortlisted antlion
   Normalize random walk and compute the location of Ant
   if Ant is available in the search dimension.
   Make the ant relocate in search dimension
   end if
   end for
   fitness factor of ants needs to be calculated
   for (each antlion)
   if the fitness factor is improved compared to antlion
   antlion eats up Ant (antlion needs to be updated)
   end if
   end for
   Update the elite antlion
End while

The updated position of the ants after ranking is given by
\[
\text{Ant}^i_k = \frac{R_k^i + R_k^i}{2},
\]  
\[\forall \in \{1, 2, \ldots, n\}.\]  

SSSEH. Relating the metaheuristic technique to the fitness function is essential for understanding the behavior of the problem and solution. Similarly to the mapping done between the algorithm based on swarm intelligence and energy-efficient CR in [37], the correlation between the metaheuristic algorithms and the fitness function becomes important (see the data in Table II below).

| S. no. | Throughput Function | MOPOSO | MOMFO | MOALO’ | RMOALO |
|--------|---------------------|--------|-------|--------|--------|
| 1      | Decision Variables Count | Swarm Behavior | Moth and flame characteristics | Ant characteristic |
| 2      | Secondary transmitter-Sensed samples | Number of particles/swarm | Number of moth and flame | Number of ants/search agents |
| 3      | Fitness function-Throughput maximization | Fitness value of swarm | Fitness of Moth position | Fitness value of Ant |
| 4      | Optimum solution-Sensing duration | Fittest particle position | Position of the moth based upon distance to flame | Elite Antlion position and its fitness value |

VI. SIMULATION RESULTS AND DISCUSSION

In this section, the throughput analysis for the separated spectrum sensing and energy harvesting scenario for the ECHRN with the proposed algorithm is confirmed by means of MATLAB simulations. The implementation was performed on a machine running the Windows 10 operating system version 21H1. It has an installed RAM of 8 GB using 11th Gen Intel(R) Core(TM) i5-1135G7 @ 2.40 GHz 1.38 GHz, 64 Bit Processor. For simulation purposes, the system parameters used are mainly derived from [14] (as shown in Table III below). The average harvested energy is taken between 0.01 µW to 0.16 µW [38].

| Symbol | Parameter | Default Value |
|--------|-----------|---------------|
| \( T \) | Duration of a timeslot | 0.1 s |
| \( E_r \) | Sensing energy | 110 mW |
| \( E_s \) | Data transmission energy | 410 mW |
| \( E_h \) | Average harvested energy | 0.01 µW to 0.16 µW |
| SNR | Signal-to-noise ratio | -15 dB |
| \( N \) | Number of sensing samples | 1000 |

The simulation settings for all five algorithms are: population size is 20, number of iterations is 500, archive size is 100, and 30 Monte Carlo trials are performed for each case. The extremely large value of this population size (e.g., 90) will increase the computational complexity of the optimization algorithms, which is undesirable. So, an intermediate value of the population is chosen.

To measure the effectiveness of the proposed rank-based multi-objective antlion optimization (RMOALO), we have considered five different test functions F1–F5. The details of the benchmark functional parameters in terms of dimensionality, search domain, and optimal global value are shown in Table IV below [39], [40]. The dimensionality exhibits the dimensions of the test functions, and the search domain marks the test area of the search space, and the
global minimum showcases the minimum value taken by the test functions to achieve convergence.

The comparative performance of the proposed algorithm and other algorithms for different test functions is given using the mean minimum, maximum, and standard deviation metrics (see data in Table V).

| Name         | Function | Dimensionality | Search Domain | Global Minima |
|--------------|----------|----------------|---------------|---------------|
| ZDT1 (F1)    | Minimize: $f_i(x) = x_i$ | 2              | [0, 1]        | 0             |
|              | Minimize: $f_2(x) = g(x) + h(f_i(x), g(x))$, where: $G(x) = 1 + \frac{9}{N-1} \sum_{i=1}^{N} x_i$ | | | |
|              | $F_i(f_i(x), g(x)) = 1 - \sqrt{\frac{f_i(x)}{g(x)}}$ | $0 \leq x_i \leq 1, \ 1 \leq i \leq 30$ | | |
| Ackley (F2)  | $f(x) = -20\exp[-0.2 \left( \frac{1}{D} \sum_{i=1}^{D} x_i^2 \right)] - \exp\left[\frac{1}{D} \sum_{i=1}^{D} \cos(2\pi x_i) \right] + 20 + \epsilon$ | 30 | [-100, 100] | 0 |
| EASOM (F3)   | $f(x) = -\cos(x_1)\cos(x_2)\exp\left[(x_1-\pi)^2 + (x_2-\pi)^2\right]$ | 2 | [-100, 100] | -1 |
| GRIEWANK (F4) | $f(x) = \sum_{i=1}^{D} \frac{x_i^2}{4000} - \prod_{i=1}^{D} \cos\left(\frac{x_i}{\sqrt{i}}\right) + 1$ | 30 | [-600, 600] | 0 |
| RASTRIGIN (F5) | $f(x) = 10D + \left[\sum_{i=1}^{D} x_i^2 - 10\cos(2\pi x_i)\right]$ | 30 | [-5.12, 5.12] | 0 |

Table V. Performance comparison of MOMFO, MOPSO, MOALO-Tournament, MOALO-Roulette wheel, and RMOALO for different test functions.

| Test Function | Algorithm                  | Mean           | Minimum         | Maximum         | Std Deviation |
|---------------|---------------------------|----------------|-----------------|-----------------|---------------|
| F1 ZDT1       | MOPSO                     | 0.4420415      | 0.0028335       | 1               | 0.274110095  |
|               | MOMFO                     | 4.276522167   | 0.301349762     | 8.789737424     | 2.15542331   |
|               | MOALO-Roulette Wheel      | 0.695312479   | 0.509284203     | 1.009716235     | 0.157357799  |
|               | MOALO-Tournament          | 0.6765339     | 0.5700102       | 1.0000000       | 0.112807534  |
|               | Proposed RMOALO           | 0.777572714   | 0.692868283     | 1.002267562     | 0.083223097  |
| F2 Ackley     | MOPSO                     | 16.437788     | 2.054921        | 21.06954613     | 5.10931771   |
|               | MOMFO                     | 20.42244285   | 2.78630012      | 22.34706961     | 4.250018151  |
|               | MOALO-Roulette Wheel      | 15.84560452   | 0.000649989     | 19.97847592     | 6.20144477   |
|               | MOALO-Tournament          | 16.20895104   | 0.038137074     | 19.99663289     | 5.509201695  |
|               | Proposed RMOALO           | 16.18311188   | 0.829809307     | 20.30860279     | 4.134937919  |
| F3 Easom      | MOPSO                     | -1.75E-22     | -6.12E-21       | 0.00E+00        | 1.03441E-21  |
|               | MOMFO                     | 2.48E-07      | -1.08E-23       | 2.48E-05        | 2.47965E-06  |
|               | MOALO-Roulette Wheel      | -0.19307025   | -0.885716657    | -2.2144E-27     | 0.295860643  |
|               | MOALO-Tournament          | -4.24E-04     | -4.24E-02       | -1.06E-27       | 0.004243454  |
|               | Proposed RMOALO           | -9.12E-03     | -4.56E-01       | -1.56E-28       | 0.0053573036 |
| F4 Griewank   | MOPSO                     | 71.39511561   | 11.14875606     | 180.0120547     | 38.55836861  |
|               | MOMFO                     | 35.68924762   | 1.299758186     | 91.13924973     | 20.76193545  |
|               | MOALO-Roulette Wheel      | 17.69652674   | 0.36679692      | 50.16619774     | 13.32720051  |
|               | MOALO-Tournament          | 11.8477996    | 0.21466434      | 50.11672004     | 10.69809831  |
|               | Proposed RMOALO           | 13.23507481   | 1.077900875     | 50.24496823     | 10.38179246  |
| F5 Rastrin    | MOPSO                     | 32.8          | 4.072911        | 57.849427       | 15.2162632  |
|               | MOMFO                     | 37.37586614   | 9.62931289      | 77.61343833     | 13.72352695  |
|               | MOALO-Roulette Wheel      | 31.01756762   | 9.370621181     | 53.47901187     | 11.50756297  |
|               | MOALO-Tournament          | 29.63183816   | 8.05109181      | 52.01330333     | 10.14598691  |
|               | Proposed RMOALO           | 16.34113611   | 4.287325569     | 62.3888473      | 11.47348816  |

Rank-based multi-objective optimization (RMOALO) shows the least standard deviation for the functions F1, F2, and F4 and is close to the lowest standard deviation for the rest of the two functions F3 and F5. On the other hand, Multi-objective moth flame optimization and multi-objective particle swarm optimization (MOPSO) have displayed relatively higher standard deviation for most of the functions. This clearly shows that rank-based multi-objective optimization has relatively high stability, thus showing robustness and consistency in its performance. Thus, it can be interpreted that the proposed RMOALO is superior or comparable to other algorithms. For any optimization algorithm, it is very important that it should not be stuck to the local optima and should converge faster.

The convergence characteristics for the benchmark test functions (F1–F5) for each algorithm are shown in Figs. 4–8 for SNR values ~15 dB. In this paper, to get a clearer view on the dependency of the fitness function on each variable,
the convergence curve is plotted for the optimum value of each variable. The convergence of the proposed algorithm is much better than the other algorithms towards the optimum value of the fitness function. Because of the rank selection method, it is able to successfully overcome the local optima and find the global optima. RMOALO can reach an optimal value in fewer iterations, also avoiding premature convergence. We have evaluated the strength and competence of the proposed RMOALO and other algorithms by applying it to the sensing duration optimization problem to achieve maximum throughput for EHCRN. The fitness function in (11) is optimized for three different values of the harvested energies. Thirty independent runs are made to eliminate any inconsistency, involving 30 Monte Carlo initial trial solutions with a randomly generated population of size 20. The maximum number of iterations is set to 1000. The performance parameters of the formulated problem have been given in terms of the mean, maximum, median, and standard deviation values of the normalized sensing duration (ratio of the sensing duration to the overall time slot) along with the mean fitness value of average throughput (data in Table VI). RMOALO is observed to provide the higher value of throughput in various iterations of the harvested energy $E_h$ at the lowest mean value of the normalized sensing duration. It is also stable in its performance, as it offers the lowest standard deviation among all other algorithms.

![Fig. 4. Convergence characteristics for ZDT1.](image)

![Fig. 5. Convergence characteristics for Ackley.](image)

![Fig. 6. Convergence characteristics for RASTRIN.](image)

![Fig. 7. Convergence characteristics for Easom.](image)

![Fig. 8. Convergence characteristics for Griewank.](image)
The convergence characteristics of the average throughput for different values of the average harvested energy ($E_h$) are shown in Figs. 9–11. The RMOALO has the ability to overcome local optima with better convergence and is successful in obtaining the best values as compared to other algorithms. The impact of normalized sensing duration on the average throughput with RMOALO reaches a maximum in a few iterations. Thus, RMOALO converges faster to get the higher fitness value.

We can see from Table VI that the behavior of the sensing duration changes with the average harvested energy in three distinct values of the harvested energy $E_h = 0.13 \mu W$, $E_h = 0.10 \mu W$, and $E_h = 0.07 \mu W$. The shorter the sensing duration, the higher the average throughput if the harvested energy is higher. As the normalized sensing duration increases, the average throughput tends to decrease. Therefore, an optimal value of sensing duration $T_2$ exists for the amount of energy harvested for which the average throughput becomes maximum. For a particular sensing time, the average throughput decreases as $E_h$ decreases. When $E_h$ is maximum, the average throughput $R_s$ attains a maximum value, and after reaching a maximum value, it decreases as there is an increase in $T_2$ and decrease in $E_h$.

To validate the effectiveness of the proposed optimization technique, a comparison of throughput maximization for the separated spectrum sensing and energy harvesting (SSSEH) scenario is also done with baseline energy-efficient spectrum sensing schemes in the cognitive radio network. The same initial setup conditions of the sensing duration $T_1 = 50 \mu s$, average harvested energy $E_h = 300 J$, the sensing
energy $E_r = 1$ J, and the energy consumed for transmission $E_t = 3$ J are considered for simulation purposes. Figure 12 shows the analysis for SNR = -28 dB. The throughput achieved using RMOALO shows 14.02 % improvement over the energy-efficient spectrum-sensing scheme - homogeneous CR and 6.74 % improvement over the energy-efficient spectrum-sensing scheme - heterogeneous CR, as shown in Table VII.

![Fig. 12. Improvement in performance using RMOALO compared to the baseline scheme.](image)

**TABLE VII. AVERAGE THROUGHPUT VERSUS NORMALIZED SENSING DURATION.**

| Scheme                                      | Maximum Throughput | Reference          |
|---------------------------------------------|--------------------|--------------------|
| Energy-efficient spectrum sensing scheme - homogeneous network | 2.64                | Table IV [26]      |
| Energy-efficient spectrum sensing scheme - heterogeneous network | 2.82                | Table IV [26]      |
| Separated spectrum sensing energy harvesting - EHCRN | 3.01                | Fig. 12            |

** VII. CONCLUSIONS**

In the separated spectrum sensing and energy harvesting cognitive radio network with the maximum throughput demands, we maximized the average throughput by optimizing the sensing duration of the ST. This has been achieved by leveraging the proposed RMOALO metaheuristic algorithm. With the SNR value of -15 dB and population size = 20, for varying the sensing time and the average harvested energy, the proposed RMOALO is 16.33 % more efficient than other metaheuristic algorithms considered.

There are several directions in which the analysis of this work could be extended. As the work considers EHCRN and metaheuristics, it can be extended from both realms for some future research, such as non-linear energy harvesting device-to-device network [41], hybrid metaheuristic optimization [42], and bidirectional networks [43].

**CONFLICTS OF INTEREST**

The authors declare that they have no conflicts of interest.

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