**Measurement of ankle joint movements using IMUs during running**

Byong Hun Kim¹², Sung Hyun Hong³, In Wook Oh⁴, Yang Woo Lee⁴, In Ho Kee⁴ and Sae Yong Lee¹,²⁺

¹ Yonsei Institute of Sports Science and Exercise Medicine (YISSEM), Yonsei University, 03722, Seoul, Republic of Korea
² Department of Physical Education, Yonsei University, 03722, Seoul, South Korea
³ Department of Sports Industry Studies, Yonsei University, 03722, Seoul, South Korea
⁴ Department of Mechanical Engineering, Yonsei University, 03722, Seoul, South Korea
⁺ Correspondence: sylee1@yonsei.ac.kr; Tel.: (+82-2-2123-6189), Fax.: (+82-2-2123-8375), corresponding authors, (SYL)

**Abstract:** Gait analysis has historically been implemented in laboratory settings only with expensive instruments, yet recently the efforts to develop and integrate wearable sensors into clinical applications have been made. Limited number of previous studies have been conducted to validate inertial measurement units (IMUs) for measuring ankle joint kinematics, especially with small movement ranges. Therefore, the purpose of this study was to validate the ability of available IMUs to accurately measure the ankle joint angles by comparing the ankle joint angles measured using the wearable device with those obtained using the motion capture system during running. Ten healthy subjects participated in the study. The intraclass correlation coefficient (ICC) and standard error of measurement were calculated for the reliability, whereas Pearson coefficient correlation was performed for the validity. The results showed that day-to-day reliability was excellent (0.974 and 0.900 for sagittal and frontal plane, respectively), and Validity was good in both sagittal (r = .821, p < .001) and frontal (r = .835, p < .001) planes for ankle joints. In conclusion, we suggest that the developed device might be used as an alternative tool to the 3D motion capture system for assessing the ankle joint kinematics.

**Keywords:** Validation; Kinematic; Inertial measurement units; motion analysis; gait

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**1. Introduction**

The ankle joint is the most frequently involved in human lower body movements, and it plays a vital role in supporting body weight by distributing gravitational and inertial loads. Once injuries, such as strain or sprain, by an external force occur in the ankle joint, it causes deformities in its structure. Impairments of the ankle joint can result in chronic ankle instability; therefore, irregular loading on one side could provoke pain on the ankle. Ankle sprains are common injuries in the general population, as well as among professional athletes [1-3]. The characteristics range from structural deficits such as joint laxity to functional impairments in gait [4]. In terms of rehabilitation, measuring the ankle joint movement pattern during ambulating or running can help clinicians determine the optimal care level a patient should receive.

Many clinical settings for gait training and rehabilitation in patients with motor impairments use a three-dimensional (3D) motion capture system considered the gold standard measurement of joint kinematics [5, 6]. The 3D motion capture system is one of the measurement tool having high accuracy, e.g., mean absolute marker-tracking errors of 0.15 mm during static trials [6] and 0.2 mm (with corresponding angle errors of 0.3) during dynamic trials [7]. A VICON system, showing high validity and reliability in
measuring joint kinematics, have been used as a suitable comparison tool to examine whether alternative systems, e.g., inertial measurement unit (IMU)-based systems, provide a sufficiently accurate method for motion analysis [8, 9]. Although this sophisticated system allows assessing kinetic and kinematic data from complicated human movements, it has several limitations. The fact that the 3D motion capture system is a marker-based system requiring many cameras is considered the primary limitation. The high cost of the instrument makes it impractical to use in various settings, such as a clinic, field, or patients’ home. Furthermore, the system cannot be used to measure and track movements simultaneously.

To overcome the limitations of the 3D motion capture system, many efforts to develop a device that can be simply conducted with concise process have been made by researchers. Recently, IMUs—a markerless motion capture technology—has been developed as an alternative measurement tool to 3D motion capture devices. IMUs is a wearable-designed device that allows sending motion measurement data to a computer in real time and giving immediate feedback (5). It collects 3D data (x, y, and z) using a combination of accelerometers, gyroscopes, and magnetometers; it is lighter, smaller, and easier to use than the 3D motion capture system. Collecting and combing raw data from multiple individual sensor are enabled by sensor fusion algorithms, and thus the estimation of 3D spherical coordinates and Euler angles in a global reference domain can be made[10].

IMUs has been evaluated and shown to be promising in estimating angular kinematics of lower limb joints, including the hip, knee, and ankle [11-13], as well as upper body posture [14]. However, as IMUs is not easily available to all professionals due to movement complexity, sensor placement, biomechanical model, and calibration procedure that could increase the risk of error of the measurement, most researchers have tried analyzing the movements of the joints conducted in the sagittal plane, such as flexion, extension, and hyperextension movements.

Especially, the errors of measurement values for the ankle in the transverse and frontal planes for gait analysis were large, which might be due to the small range of motion in these planes or the differences in the anatomical or biomechanical definitions between the two systems [15]. However, to our best of knowledge, the number of previous studies investigated angular kinematics of the ankle joint are limited, and it is necessary to establish validity as a clinical tool to aid in the diagnosis of gait impairment and treatment. Therefore, the purpose of this study was to verify whether the newly developed device can be simply operated with high accuracy and concise calibration process.

2. Materials and Methods
2.1. Participants and data collection

Ten healthy male participants (26.5±6.3 years, 75.12±19.33 kg) were recruited in this study. Exclusion criteria for the study were as follows: individuals who had ankle surgery or nervous system damage or disorder and those with any injuries to the lower limbs within the past three months that could affect the neuromuscular function. The study protocol was approved by the Office of Research Ethics at Yonsei University (IRB No. 7001988-202101-HR-1076-03) and all subjects provided an informed consent.

2.2. IMU system and sensor placements

A Raspberry Pi 3 Model B+ computer and two Adafruit BNO055 IMUs sensors were used (Adafruit, New York, USA) for data collection. Sensor data were collected at a constant frequency of 100 Hz. One IMUs sensor was placed on top of the instep of the right foot (Sensor 1), and the second IMUs sensor was tightly fixed on the right shin (Sensor 2) using a specially designed holder. The sensors were required to be perfectly parallel to each other as well as the ground for accurate calculations. Thus, we designed a
shoe mount for Sensor 1 and a sensor holder with a strap for Sensor 2. Both parts comprised a set of an acrylic sensor slide plate and acrylic holder for easy detachment during the calibration process. In addition, we mounted four-corner leveling systems on both holders for leveling. Sensor 2 was fixed as reference coordinates by built-in coordinates (ref-coordinates) of BNO055 IMUs sensor. Eulerian displacements were calculated by subtracting Sensor 1 coordinate data (test-coordinate) from ref-coordinate values. Displacement values of each axis were referred to the yaw, pitch, and roll status, respectively.

2.3. Vicon system and marker placement

The kinematic data were collected in 100 Hz and their positions targeted capture volume. The calibration of Vicon system were conducted before each data collection. Plug-in-Gait (PiG) lower body model was used to analyze movement at the ankle joints. A total of reflective 16 markers were placed on the participants before testing, and a static calibration trial was initially collected to form a musculoskeletal model based on (Figure 1) an 8-camera motion analysis system (VICON, Oxford, UK). The place of markers was attached to the following landmarks: ASIS, PSIS, mid-lateral thigh, lateral knee joint line, lateral mid-shank, lateral malleoli, calcaneal tuberosity and head of the second metatarsal. The participants were measured the specific information of weight, height, ankle width, knee width, and leg length in the lower body model. Figure 1 shows the participants’ set up of the anterior, lateral, and posterior views with the markers in place. Pig model of Vicon was sued for evaluating all parameters. The lower body was modeled as seven segments (one pelvis, two thighs, two shanks, and two feet). A normal gait cycle was defined from the initial heel-to-heel contact with the same limb.

2.4. IMUs joint angle calculations

The proposed IMUs sensor includes internal algorithms to calibrate the gyroscope, accelerometer, and magnetometer inside the device. The calibrations of gyroscope, accelerometer, and magnetometer were conducted at the same time that investigator held the device with hand and shook it shaping the figure 8. However, the IMUs sensor did not contain any internal electrically erasable programmable read-only memory, so we had to perform the formal calibration process every time the device started up.

![Figure 1. Participants’ set up](image)

After the calibration, raw sensor orientation data were received as types of quaternions. These quaternions needed to be converted to an Euler angle, commonly used units, for easy comprehension. Euler angles were obtained from the quaternions via the equations [16]:

\[ \text{Euler angles} = \text{quat2euler}(\text{quat}) \]
\[
\begin{bmatrix}
\varphi \\
\theta \\
\psi
\end{bmatrix} =
\begin{bmatrix}
\arctan \frac{2(q_0q_1 + q_2q_3)}{1 - 2(q_1^2 + q_2^2)} \\
\arcsin(2(q_0q_2 - q_3q_1)) \\
\arctan \frac{2(q_0q_3 + q_1q_2)}{1 - 2(q_2^2 + q_3^2)}
\end{bmatrix},
\]

\[
q_0 = q_w = \cos (\alpha/2) \\
q_1 = q_x = \sin (\alpha/2) \cos (\beta_x) \\
q_2 = q_y = \sin (\alpha/2) \cos (\beta_y) \\
q_3 = q_z = \sin (\alpha/2) \cos (\beta_z)
\]

where \(\varphi, \theta,\) and \(\psi\) are Euler angles and \(q_0, q_1, q_2,\) and \(q_3\) are quaternions. \(\alpha\) is a simple rotation angle and \(\cos (\beta_x), \cos (\beta_y),\) and \(\cos (\beta_z)\) are the direction cosines (Euler's rotation theorem).

The coordinate system of the IMUs sensor was aligned parallel to the floor, and the angle started at 0 degrees based on that state. As the sensors and ground were started parallelly (Figure. 2), ankle motion was generated by simply subtracting Sensor 1 (ref-coordinate) and Sensor 2 (test-coordinate) angles. The static angle value was added to the subtracted value of the IMUs sensor.

![Figure 2. Sensor placement](image)

Description of the location of each IMUs sensor (red), Raspberry Pi (yellow), and PiG body model marker location for the: (left) anterior view; (middle) lateral view; and (right) posterior view.

2.5. Vicon joint angle calculations

Kinematics of the ankle joint were measured using Vicon PiG model. Sagittal plane motion of the ankle is taken between shank anterior to posterior axis and the projection of the axis formed by the heel and toe markers into the sagittal plane of the foot. Furthermore, frontal plane motion of the ankle is taken between the ankle medial to lateral axis and projection of the axis formed both malleoli. Additional information of PiG angle calculations is on Vicon’s website. ([https://docs.vicon.com/display/Nexus26/Full+body+modeling+with+Plug-in+Gait](https://docs.vicon.com/display/Nexus26/Full+body+modeling+with+Plug-in+Gait)).

2.6. Experiment protocol

To evaluate the validity between VICON and IMUs for ankle movements, a functional movement protocol was generated. Along with the reflective markers, two wearable IMUs sensors were attached to participants. Participants were asked to perform a running task. Initially, they were instructed to naturally walk to synchronize the position of the markers and sensors as the zero spots and then to try running. The peak point [maximum dorsiflexion (Max DF) to Max DF] of this movement was detected to
synchronize the two systems. Participants performed the running task. The data recording protocol consisted of five trials of running (2.68 m/s). Prior to test, all participants were given time to 10-min of warm up and familiarization session, and asked to have a rest of 2 minutes between each trial.

2.7. Data processing and statistical analysis

The motion capture data were considered the gold standard reference for kinematic data for this study. Data from the IMUs and VICON were synchronized by matching them based on the positive peak of the measure by each system [17]. The marker trajectories were imported to Matlab, and joint angles were computed and filtered with Matlab. The five cycles from Vicon and IMUs were synchronized using the positive peak value in the sagittal and frontal planes. The raw data were filtered by a fourth-order Butterworth low-pass filter with a cut-off frequency of 6 Hz, following the recommendation of previous studies [18], to attenuate unwanted noise. Data analysis was performed in Matlab software for running for both sagittal and frontal planes of movement. All data were calculated as averages of all repetitions before being averaged across all participants. All statistical analyses were conducted using SPSS ver. 25.0 (IBM, Armonk, NY, USA). For the test–retest, the intraclass correlation coefficient (ICC) was calculated for each plane of the ankle joint during running for each two systems respectively [19]. Pearson coefficient correlation was performed to verify the relationship of ankle angle between IMUs and VICON in the sagittal and frontal planes.

3. Results

3.1. Demographics and descriptive

Ten male participants (means ± standard deviation age: 30.2 ± 5.3 years; height: 171 ± 15.3 cm; body mass: 73.6 ± 12.4 kg) were enrolled in the study. Confirmed the consent forms were given from the all participants. A total of 50 trials (running task; five trials per subject) were conducted and analyzed.

3.2. Reliability (test–retest)

The test–retest reliability of the IMUs in measuring the sagittal and frontal planes with ICC, and its standard error of measurement (SEM) is described in Table 1. A high correlation with ICC (2, 1) values of 0.974 and 0.9 for the sagittal and frontal planes were observed, respectively.

| Static measurement | Sagittal plane (ICC) | Frontal plane (ICC) | SEM |
|-------------------|----------------------|---------------------|-----|
| VICON             | 0.978                | 0.969               | 0.39|
| IMUs              | 0.974                | 0.9                 | 4.89|

ICC: intraclass correlation coefficient; SEM: standard error of measurement

3.3. Validity (Pearson coefficient correlation)

The validity test for ankle dorsiflexion/plantarflexion and eversion/inversion is shown in Table 2. Figure 3 and 4 present the sagittal and frontal angles obtained from VICON and IMU systems during the running task. All planes showed high validity between the pattern of sagittal ($r = .821, p < .001$) and frontal ($r = .835, p < .001$) angles provided by the two systems.
Table 2. Pearson coefficient correlation of sagittal and frontal planes (IMU-based system)

| Measurement   | Sagittal plane | Frontal plane |
|---------------|----------------|--------------|
| VICON vs IMUs | 0.821**        | 0.835**      |

**p < .001

Figure 3. Comparison of ankle angle between VICON and IMUs in the sagittal plane

Figure 4. Comparison of ankle angle between VICON and IMUs in the frontal plane

4. Discussion
The primary aim of this study was to validate IMUs measurement in the sagittal and frontal plane joint kinematics with the VICON system during running. The newly developed IMUs showed excellent reliability between the test and re-test measurements (ICC = X; 0.974, Y; 0.9). The ICC values for kinematic parameters were generally higher or equal to those in other studies, which only assessed reliability during simple planar movements, such as the sagittal plane [12, 15, 20-22]. In addition, validity described as a correlation of the joint angles measured by the two systems was significantly high in the sagittal plane (r = 0.821, p < 0.01) and frontal plane (r = 0.835, p < 0.01) during running.

Previous studies have reported moderate to high validity of IMUs for measuring simple movement but showed low and varied to moderate values for complex movements, such as jumping and running, which may be because the complexity of the movements causes a problem for devices in transmitting and receiving data. Meanwhile, previous studies used the frequency-hopping spread spectrum function of Bluetooth to transmit data [23], we tried increasing communication range by using a direct sequence spread spectrum with Wi-Fi to prevent data transmission issues. Further, compared with low-power devices, the newly developed device showed high accuracy in collecting data by having 54 Mbit/s of transmission speed [24]. Although many efforts to improve the accuracy of data transmission functions of sensors have been made, the limitation of the place where it could be applied persists. However, with Raspberry pi, a function of acquiring and saving rapidly varying time-signal with high frequency [25, 26], system-on-chip, which enables the device to save data to its memory room made it possible to be used in various outdoor sports.

In terms of the validity related to the specific movement—running, in this study—we chose the conventional gait model (PiG) to investigate the relationship between the newly developed device and VICON. One possible limitation of the proposed model is the different location of marker placement on a calculated joint angle, which is used to define the internal and external rotation of the tibia against the line of the ankle joint center, could cause appreciable errors in ankle joint kinematics, especially the frontal and transverse planes [27]. Regarding this, we devised a similar environment as a marker-based system to reduce errors between devices. The sensors were positioned perfectly parallel to each other as well as the ground using a mini-inclinometer for accurate calculations. The results showed that IMUs seemed to be a suitable alternative to motion capture systems in both dorsiflexion/plantarflexion and eversion/inversion movements at the ankle joint during the running task [X: 0.821, Y: 0.835].

High accuracy for assessing the ankle joint movements in the sagittal and frontal planes was a different result from other previous studies [12, 22]. According to previous studies, the poor correlation between VICON and IMUs in measuring inversion and eversion was higher than dorsiflexion and plantarflexion due to its smaller range of motion. Specifically, they reported that if the complexity of movement increases, validity would decrease. In addition, most of them used only simple planar movement protocols, such as isolated flexion-extension, which limited the generalizability of their conclusions. Our results extend these previous findings by considering a more challenging task: running.

As complex movements occurred at more than a single plane and with irregular movement velocity affect system performance [28, 29], an accurate method for proper calibration (proper alignment of the IMUs axes with the anatomical segment axes) is considered to be another essential factor contributing to reliability due to different calibration protocols may result in substantially different consequences [30]. Many previous studies did not identify or sufficiently describe their calibration procedure.

In clinical settings, IMUs has been suggested as an alternative tool to the 3D motion capture system, because it provides real-time data in functional tasks within the same error range compared to classical measurement devices. Although it offers convenience in measurement, probably it may make the users to take more time and technical resources to assess patient until the system becomes more user friendly. The development of IMUs will make it possible to provide valid data to assess the range of motion and joint
orientation, and therefore, rehabilitation research and healthcare services will benefit from IMUs. We conducted our validation study with healthy subjects to reduce the error of validity, yet IMUs need to ultimately benefit pathological populations and clinicians by guiding the clinical decision making [31]. Therefore, in the future study, special considerations will be needed in pathological populations, as most calibration procedures require specific posture or movement. [32].

5. Conclusions

We developed a system to measure the ankle joint angle using IMUs sensors which is convenient, inexpensive (approximately $300), light, and portable. Furthermore, it has a function of communicating with a computer via Bluetooth, and the computer is able to immediately calculate the data by Phython. In order to validate the device, we compared the ankle X and Y angles data obtained from the IMUs with that acquired from the VICON system. The result of comparison indicates that the IMUs and motion capture systems deviated a level precision that is well below normal measurements performed in a clinical setting. In the future, we will extend this approach and thus, apply to the IMUs-based training that is providing multiple body joint angle kinematics in real time.

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