Constraint on precipitation response to climate change by combination of atmospheric energy and water budgets

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Global mean precipitation is expected to increase with increasing temperatures, a process which is fairly well understood. In contrast, local precipitation changes, which are key for society and ecosystems, demonstrate a large spread in predictions by climate models, can be of both signs and have much larger magnitude than the global mean change. Previously, two top-down approaches to constrain precipitation changes were proposed, using either the atmospheric water or energy budget. Here, using an ensemble of 27 climate models, we study the relative importance of these two budgetary constraints and present analysis of the spatial scales at which they hold. We show that specific geographical locations are more constrained by either one of the budgets and that the combination of water and energy budgets provides a significantly stronger constraint on the spatial scale of precipitation changes under anthropogenic climate change (on average about 3000 km, above which changes in precipitation approach the global mean change). These results could also provide an objective way to define the scale of ‘regional’ climate change.

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INTRODUCTION

Improving our understanding of the response of the hydrological cycle to climate change is key to effective adaptation strategies—and remains a major scientific challenge. As the global mean temperature increases with changing climate, the global mean precipitation rate is predicted to increase by about 1–3% K\(^{-1}\). This rate of increase in precipitation is slower than the rate of increase in humidity in the atmosphere due to thermodynamic considerations (which is predicted to be \(-7\%\) K\(^{-1}\) from the Clausius–Clapeyron relation). The slower rate of precipitation increase compared to the humidity increase is due to energetic constraints\(^4,5\), i.e. the ability of the atmosphere to radiatively cool, and must impose a decrease in convective mass fluxes\(^1\). Compared to the global mean response, regional changes in precipitation remain poorly understood\(^2\). At what scale do precipitation changes transition from global (or large-scale) to regional precipitation changes values? We note that previously ‘regional’ and ‘global’ has generally not been objectively defined in this context.

Any global or local precipitation change is constrained by both the atmospheric energy budget\(^4,6,7\) and the atmospheric water budget\(^8,9\). The atmospheric energy budget forces any global mean precipitation increase (which increases the latent heat release) to be balanced by an increase in the radiative cooling of the atmosphere and/or by a decrease in the surface sensible heat flux. Locally, the increased latent heating could be compensated by changes in the divergence of dry static energy\(^8,10,11\), which was shown to exhibit contrasting behaviour for tropical and extra-tropical perturbations\(^12\). A similar argument could be presented for the atmospheric water budget, i.e. globally, any increase in precipitation must be accompanied by a similar increase in evaporation. Again, local precipitation changes could be compensated by changes in the divergence of water vapour\(^8\). Changes in the divergence of water vapour could be induced by either changes in atmospheric circulation, driving changes in air mass divergence (referred to as the dynamical contribution), or by changes in the water vapour capacity, driving changes in the divergence of water vapour, even for a given air mass divergence (referred to as the thermodynamically contribution\(^13\)). The latter is expected to follow the Clausius–Clapeyron relation.

On long time-scales (for which atmospheric storage terms can be neglected), the vertically integrated energy and water budgets are given, respectively, by:

\[
P + Q = \text{div}(s), \tag{1}
\]

\[
P - E = -\text{div}(q_v), \tag{2}
\]

where \(P\) is the precipitation, \(E\) is the evaporation and \(\text{div}(s)\) and \(\text{div}(q_v)\) are the divergence of dry static energy \(s\) and water vapour \(q_v\), respectively (in units of W m\(^{-2}\)). \(Q\) is the sum of the surface sensible heat flux \(\text{Q}_{\text{sw}}\) and the atmospheric radiative heating \(\text{Q}_{\text{h}}\) due to radiative shortwave (SW) and longwave (LW) fluxes \(F\). \(Q_h\) can be expressed as the difference between the top of the atmosphere (TOA) and the surface (SFC) fluxes as follows:

\[
\text{Q}_h = (F_{\text{SW}}^{\text{TOA}} - F_{\text{SW}}^{\text{SFC}}) - (F_{\text{LW}}^{\text{TOA}} - F_{\text{LW}}^{\text{SFC}}), \tag{3}
\]

where LW fluxes are positive upward and SW fluxes are positive downward.

Recent research has demonstrated that under our current climate conditions the atmospheric water and energy budgets are locally closed on scales of the order of 4000–5000 km\(^8\). That means that, based on observations in the tropics, once averaged over \(-5000\) km \(P \approx Q\) and the atmosphere is close to radiative-convective equilibrium\(^5,14\). In addition, based both on climate model and reanalysis data-sets it was shown that a similar averaging scale \((\sim 4000\) km\) is required to close the water budget (i.e. \(P \approx E\))\(^8\). Beyond these scales, the divergence terms become inefficient in compensating the energy/water imbalance.

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Shifting our perspective from the current climate to a changing climate, Eqs. (1) and (2) become:

\[ \delta P + \delta Q = \delta \text{div}(s); \]
\[ \delta P / C_0 = \delta \text{div}(q_v); \]

where \( \delta \) represents the difference between a future climate and the current climate. Previous work demonstrated that the correlation between \( \delta P \) and \( \delta E^8 \) and between \( \delta P \) and \( \delta Q^6 \) increase with the spatial scale of averaging and becomes larger than 0.5 for a scale of a few 1000 km. This again demonstrates that the ability of divergence to compensate for changes in precipitation decrease with the spatial scale. Once the divergence terms become inefficient, the precipitation changes approach the global mean change, which is known to be relatively small (compared to local precipitation changes—1–3% K\(^{-1}\))\(^{1,2}\). However, precipitation changes on regional scales, for which the divergence terms remain efficient, could be much larger than the global mean. Hence, identifying the ‘break-down’ scale between these two regimes can help in understanding and predicting future changes in precipitation. A priori, the decrease of efficiency of divergence with averaging scale does not have to be similar for the water and energy budgets. In addition, at different geographical locations the relative magnitude of the two divergence terms could change. Thus, it is possible that the characteristic spatial scale of changes in precipitation under global warming is constrained by a combination of the atmospheric energy and water budgets with a changing relative importance between them. We note that the relative role of the different budgets has not been quantified before. The aim of this study is to examine the differences and commonalities between the water\(^8\) and energy\(^6\) budgets control on precipitation and their role in determining the spatial scale of changes in precipitation under climate change. We demonstrate that combining the water and energy budget constraints results in improved predictions of the scale of precipitation changes.

**RESULTS**

Energy and water budgets control on precipitation

Figure 1 presents the multi-model mean divergence terms of both the water and the energy budgets, averaged over different spatial scales. In the tropics the two divergence terms are strongly anti-correlated and show the same spatial structure (please note that \( \text{div}(q_v) \) is presented with a minus sign to be consistent with...
Eqs. (1) and (2). The multi-model mean spatial correlation between \(-\text{div}(q_v)\) and \(\text{div}(s)\) in the tropics (\(-30^\circ\) to \(30^\circ\)) is 0.94 (see Supplementary Fig. S1, for the zonal mean behaviour of all models). The high correlation in the tropics demonstrates that any convergence of water vapour that generate precipitation will be accompanied by production and divergence of dry static energy. The opposite is true in the sub-tropics where there is a net divergence of water vapour and a net convergence of dry static energy. Moving poleward, \(\text{div}(s)\) becomes negative and large (in absolute magnitude), while \(-\text{div}(q_v)\) becomes positive and small. At high latitudes, there is a net convergence of both water vapour and dry static energy as both are being advected from lower latitudes by eddies. However, as the amount of water vapour decreases with the decrease in temperatures towards the poles, the convergence of water vapour decreases from the mid-latitudes storm tracks to the poles. In contrast, the dry static energy convergence increases pole-wards. The zonal mean divergence terms of water vapour and dry static energy reflect the meridional advection of moist static energy\(^{15}\). We note that at the native resolution (upper row) the divergent terms appear small at many locations especially over land; however, they are not negligible compared to the local precipitation (see Supplementary Fig. S2 presenting the normalised divergent terms).

Averaging the water vapour and dry static energy divergence terms over increasingly larger scales (Fig. 1), we note that the spatial pattern becomes weaker and almost completely vanish at 3000 km. This weakening of the spatial pattern occurs on smaller scales for the water budget (c.f. Dagan et al.)\(^8\) than for the energy budget.

This weakening of the spatial pattern occurs on smaller scales for the pattern becomes weaker and almost completely vanish at 3000 km. For the energy budget it is accompanied by production and divergence of dry static energy. The opposite is true in the sub-tropics where there is a net convergence of both water vapour and the energy budgets is large due to the large role of advection of water and energy from lower latitudes.

On average \(\mathcal{L}_{WB} > \mathcal{L}_{EB}\) due to the larger variance in \(E\) compared to \(Q\), which more effectively counteract the large variance in \(P\) (see Supplementary Fig. S3). However, at different regions the ratio between \(\mathcal{L}_{EB}\) and \(\mathcal{L}_{WB}\) changes (Fig. 2c). For example, at high latitudes \(\mathcal{L}_{WB} > \mathcal{L}_{EB}\) everywhere, while at mid-latitudes (around \(\pm40^\circ\)) \(\mathcal{L}_{EB}\) is generally smaller than \(\mathcal{L}_{WB}\) over the oceans but less so over land (for which almost at all latitudes \(\mathcal{L}_{EB} > \mathcal{L}_{WB}\)). Over the tropical oceans we note a difference between the Atlantic and the eastern part of the Pacific, for which \(\mathcal{L}_{EB} < \mathcal{L}_{WB}\) and the west Pacific and the Indian ocean for which \(\mathcal{L}_{EB} > \mathcal{L}_{WB}\). For the latter, the existence of the warm pool and associated cloud cover releases a significant amount of latent heat by precipitation, which cannot be compensated locally by the relatively small radiative term.

Although both budgets are contributing to constrain precipitation, we expect that the smaller scale between \(\mathcal{L}_{EB}\) and \(\mathcal{L}_{WB}\) (locally) would be the limiting factor and will determine the spatial scales of changes in precipitation in future climate. Hence, we combine \(\mathcal{L}_{EB}\) and \(\mathcal{L}_{WB}\) to a single scale \(\mathcal{L}_{WB:EB}\), which is \(\mathcal{L}_{WB:EB} = \min(\mathcal{L}_{WB}, \mathcal{L}_{EB})\) (Fig. 2d).

As was shown in Dagan et al.\(^8\), the average scale required for closure of the water budget depends on the definition of closure, or to within what percentage \(P\) is close to \(E\). The same is true for the energy budget (Fig. 3). A stricter closure requires larger scale of averaging for both the water and the energy budgets. We also note that for both budgets the scale for closure in the tropics is smaller than the global mean scale. This is again due to the large contribution of advection of water vapour and dry static energy from low to high latitudes. In addition, on the global mean \(\mathcal{L}_{EB} > \mathcal{L}_{WB}\) for all the levels of closure. As expected, the combined scale, \(\mathcal{L}_{WB:EB}\) has a smaller mean for all the levels of closure (as it is defined as the minimum of \(\mathcal{L}_{EB}\) and \(\mathcal{L}_{WB}\) for each location, Fig. 3). We note that the mean values of \(\mathcal{L}_{EB}\) and \(\mathcal{L}_{WB}\) presented here based on climate models are consistent with previous estimates based on observations\(^{14}\).
Fig. 3 Average scale of closure of the water and energy budgets and of precipitation changes. The multi-model mean spatial scale for local water budget closure ($L_{WB}$—for which precipitation roughly equals evaporation), energy budget closure ($L_{EB}$—for which precipitation roughly equals the sum of the atmospheric radiative heating rate and surface sensible heat flux), the combined water and energy budget scale ($L_{WB+EB}$) and the scale of changes in precipitation ($L_P$) as a function of the degree of closure or relative precipitation change. As all quantities are normalised locally by historical $\mathcal{P}$ (Eqs. 6–8), the $x$-axis represents a similar amount of water for all. The global mean and the tropical mean are presented for each scale. The vertical lines represent the standard deviation of the 27 different CMIP5 models.

The average scale of precipitation changes under climate change ($L_P$) is also presented in Fig. 3. The scale of precipitation changes is calculated as the scale for which the relative precipitation changes (as absolute value) is smaller than a given value, $R$:

$$|\Delta P/P| < R,$$

for $R$ in the range of 7.5–15%. We note that the level of imbalance in the different budgets for a given closure threshold is similar (in terms of water amount) to the magnitude of the relative precipitation change $R$, as all are normalised by the (same) local historical precipitation (Eqs. 6–8).

Figure 3 demonstrates that the combined scale $L_{WB+EB}$ is more similar to (but slightly larger than) $L_P$ than either $L_{EB}$ or $L_{WB}$ separately. This is also demonstrated in Fig. 4 which presents the multi-model mean $L_{WB}$ vs. $L_{EB}$, $L_{WB+EB}$ and $L_P$ for different levels of closure. Figure 4 demonstrates that $L_{WB}$ is much larger than $L_{EB}$ for all levels of closure. The same is true for $L_{WB}$ but to a lesser extent, and the combined scale ($L_{WB+EB}$) is the closest to $L_P$. These results demonstrate that combination of water and energy budgets provides a better constraint on the scale of precipitation changes under climate change (2500–3000 km for a 10% combined budget imbalance or relative precipitation change). Above this scale, precipitation changes approach the global mean change (usually on the order of a few percent), while below it they could be substantially larger.

DISCUSSION

Global mean precipitation changes due to global warming are predicted to be relatively small ($-3\% \text{ K}^{-1}$) compared to the rate of increase in atmospheric water vapour ($-7\% \text{ K}^{-1}$). Any global mean precipitation change must be consistent with both the atmospheric energy and water budgets, meaning that precipitation must change such that the atmospheric energy and water budgets remains in balance [17–19]. Local precipitation changes could be compensated for by divergence of water vapour or dry static energy [15,11] and hence could be much larger than the global mean change. Previous studies have accounted for the changes in the divergence term of the energy budget to understand precipitation changes due to different drivers [15,11]. However, these divergence terms are expected to become less efficient with increasing scales and must vanish on the global scale. While both the energy and water budget constraints on precipitation are well studied individually [10,11,16,17], their relative importance for different regions has not been well evaluated. In addition, the spatial scales at which each constraint holds has not been thoroughly quantified. Hence, most previous studies made arbitrary definitions of 'regional' vs. 'large-scale' precipitation change. Using 27 CMIP5 models we identify the scale for which the divergence terms become inefficient and above which the changes in precipitation are expected to approach the global mean change to be about 2500–3000 km. This could provide an objective way to define the scale of 'regional' climate change. We note that a shift in the precipitation spatial pattern under climate change (such as a shift in the location of the inter-tropical convergence zone or a widening of the Hadley cells) could also be interpreted as a shift in the water and energy divergence terms. For example, in the tropics the scale of closure of the different budgets is roughly determined by the scale of the Hadley cells (averaging the sub-tropical net evaporation/radiative cooling regions with the net precipitation regions of the deep tropics—Fig. 1). Hence, the future predicted widening of the Hadley cell [18] is expected to enlarge the budget closure scales. However, we note that the Hadley cell is expected to widen by about 100–200 km [8], while the scale of closure of the different budgets is at the order of 4000–5000 km. Hence, we do not expect this widening to significantly affect our results. This can also be seen from Dagan et al. [4], which showed that the scale of closure of the water budget is not expected to change significantly in future climate compared to the inter-model spread. In addition, we note that the change in the mean location of the inter-tropical convergence zone due to aerosol forcing is expected to occur on much smaller scales than the closure scales presented here.

Here we show that the characteristic scale of precipitation changes under anthropogenic climate change is better...
constrained by a combination of the water and energy budgets than by each one separately. This demonstrates that combining the water and energy budget perspective will improve our understanding of the drivers behind, and the scale of septation of, local and large-scale precipitation changes.

METHODS
CMIP5 data

The analysis is based on data from 27 CMIP5 (phase 5 of the Coupled Model Intercomparison Project5) models (listed in Supplementary Table 1) for the following two protocols: historical and RCP8.5 (Representative Concentration Pathway 8.5—a scenario with relatively fast increase in greenhouse gas concentrations) simulations. From the historical runs we average the data over the last 20 years of the 20th century, while from the RCP8.5 runs we average the data over the last 20 years of the 21st century. Changes in precipitation (ΔP) are determined based on the difference between the RCP8.5 and the historical runs. All data are remapped to T63 resolution (about 1.8°). The divergence terms (of either the water or the energy budget) are calculated as the residual of the other terms. We note that, in climate models, the water and energy budget constraints (Eqs. (4) and (5)) hold to the degree the models conserve terms. We note that, in climate models, the water and energy budget constraints (Eqs. (4) and (5)) hold to the degree the models conserve terms. We note that, in climate models, the water and energy budget constraints (Eqs. (4) and (5)) hold to the degree the models conserve terms.