Hybrid Tamm plasmon resonance excitation towards a simple and efficient biomedical detector of NaI solution

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This work presents a theoretical verification for the detection of Sodium iodide (NaI) solution with different concentrations in the vicinity of Tamm plasmon (TP) resonance. The proposed sensing tool is constituted of (prism/Ag/cavity/(GaN/CaF2)15/air). The essential foundation of this study is based on the displacement of the TP resonance by varying the concentration of an aqueous solution of sodium iodide (NaI) that fills the cavity layer. The resonant TP dip is shifted downwards the shorter wavelengths with the increment of the Ag layer thickness. Nevertheless, the resonant TP dip is shifted upwards to longer wavelengths with the increment of NaI refractive index/concentration. Also, the sensitivity of the sensing tool decreases with the increment of the NaI refractive index. However, the minimum result is not less than the value of 9913 nm RIU$^{-1}$ for a concentration of 25%. Finally, the performance of our sensor in the form of the quality factor, detection limit, and figure of merit showed significant improvements in designing a high-performance liquid and biosensor.

1. Introduction

The scientific and industrial communities are always working on the design and fabrication of stable and reliable sensing devices applicable for monitoring many physical, biological, and chemical phenomena. In recent years, optical-based sensors received considerable attention as a result of their low cost, high levels of safety and also high efficiency. In this regard, these types of sensors are mainly designed and fabricated based on the changes in optical characteristics such as reflectivity, transmittivity, and absorbance. These changes could be generated as a result of specific chemical, physical or biological characteristics. Therefore, many of the complex interactions could be simply analyzed and clarified using these simple instruments.

In this context, the excitation of Tamm plasmon (TP) resonance at the interface between a thin metallic layer of definite thickness and a multilayer periodic structure like photonic crystals (PCs) could be the mainstay for the above-mentioned sensors. Hence, PCs as artificial periodic designs in one, two, or three dimensions are capable of the formation of some stop frequency bands along the spectrum of the incident electromagnetic waves. These bands are likely defined as photonic band gaps (PBGs). In addition, PCs with a broken periodicity have significant progress through the process of photon localization. Thus, the appearance of the PBGs and photon localization grants PCs more sparkle to be the mainstay in many different applications. PCs are designed and fabricated for optical switches and reflectors, communication systems, camouflage, renewable energy and solar cells, and chemical, physical, and biomedical sensors. However, the transmittivity of PC structures including resonant peaks has a limited response to the variations of some physical, chemical, or biological parameters like temperature, pressure, and concentration. Therefore, the creation of TP resonance through PC designs could offer a significant response to this limited response. In particular, TP resonance is characterized by a relatively high sensitivity against any biological, physical, or chemical variations. Meanwhile, the presence of wide PBGs leads to some flexibility in the creation of TP resonance modes without any coupling with other resonant modes. In this regard, the excitation of TP resonance modes based on PC structures received considerable attention on both theoretical and experimental levels. In this research, we intend to present a theoretical verification for the detection of NaI solution with different concentrations in the vicinity of TP resonance. Also, this research study is introduced for sensing NaI concentrations due to the significant importance of NaI in

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many fields. Notably, NaI is of great potential interest through nuclear medicine diagnostics.\(^{41}\) Meanwhile, NaI has a significant role in the scintigraphy and therapy of the thyroid gland beside the biosynthesis of thyroid hormone.\(^{42}\) In addition, the treatment of iodine deficiency due to poor nutrition could be investigated using a solution of NaI mixture.\(^{43}\) For the monitoring of NaI, we have designed a cavity layer between a thin layer of Ag metal with the thickness \(d_a\) and a one-dimensional PC structure. Then, the suggested design is enclosed by a prism on its top surface to enhance the total reflection through the design and a substrate from the air on its bottom surface. Therefore, the proposed sensing tool is constituted as, \{prism/Ag/cavity/(GaN/CaF\(_2\))\(^{15}\)/air\}. The essential foundation of this study is based on the displacement of TP resonance modes by changing the aqueous NaI concentrations through the cavity layer. Firstly, the cavity layer is filled with the pure water solution, so the TP resonance mode appears at a specific wavelength. As the water solution inside the cavity is replaced with NaI solution with different concentrations, the TP resonant mode will be displaced to new wavelengths. Therefore, the detection of NaI could be investigated relative to the shift in TP resonance positions. The numerical results are demonstrated in the vicinity of the transfer matrix method (TMM). For the best possible performance of this sensing tool, a wide optimization procedure for the thicknesses of the cavity and Ag layers and angle of incidence is investigated.

2. Sensor design and theoretical analysis

In what follows, we describe the suggested design of our proposed sensor. Fig. 1 shows the schematic representation of this sensor in which the cavity layer of a definite thickness \(d_c\) is dipped in between a thin layer of Ag metal with the thickness \(d_a\) and a one-dimensional PC structure. Here, the one-dimensional PC structure contains 15-unit cells each of them composed of gallium nitride (GaN) and calcium fluoride (CaF\(_2\)) with thicknesses \((d_c)\) and \((d_d)\), respectively. Then, a prism and substrate from the air are surrounding the proposed design.

To simulate the route of the incident electromagnetic waves through the suggested design, the Transfer Matrix Method (TMM) is used. In fact the TMM is investigated to describe the response of the electric and magnetic fields through the multilayer structures as a function of the wave vector, refractive indices, and thicknesses of the constituent materials.\(^{44-46}\) Then, the result of this perception appears in the form of a \(2 \times 2\) matrix. Finally, the optical characteristics of the designed structure such as transmittivity and reflectivity could be obtained in the vicinity of the basic elements of this matrix. In this regard, through a given direction \((Z)\) as the direction of propagation, the electric and magnetic field’s components for the TE mode of polarization are described as:\(^{44-46}\)

\[
E_j(z) = U_j \exp(-ik_jz) + V_j \exp(ik_jz) = E_{j+} + E_{j-} \quad (1a)
\]

\[
H_j(z) = -i \frac{\alpha_j}{\omega} \frac{\partial E_j}{\partial z} = -k_j \frac{\alpha_j}{\omega} \left[ -U_j \exp(-ik_jz) + V_j \exp(ik_jz) \right] \quad (1b)
\]

With \(k_j = k_0 n_j \cos \theta_j = \left( \frac{2\pi}{\lambda} \right) (n_j \cos \theta_j)\) to define the wave vector component along the \(Z\) direction as a function of the incident angle \((\theta_j)\), the refractive index \((n_j)\) and the wavelength of the incident radiation \((\lambda)\), then, \(U_j\) and \(V_j\) as the amplitudes of the fields components. Now eqn (1b) can be written in a more generalized form in the vicinity of eqn (1a) as:

\[
H_j(z) = k_j \frac{\alpha_j}{\omega} \left[ E_{j+}, E_{j-} \right] = \zeta_j \left[ E_{j+}, E_{j-} \right] \quad (2)
\]

Then, the combination of eqn (1) and (2) can lead to the following matrix formalism:

\[
\begin{pmatrix}
E_j(z) \\
H_j(z)
\end{pmatrix} = \begin{pmatrix}
1 & 1 \\
\zeta_j & -\zeta_j
\end{pmatrix} \begin{pmatrix}
E_{j+} \\
E_{j-}
\end{pmatrix} \quad (3a)
\]
With,
\[
\begin{pmatrix}
E_{x,+} \\
E_{y,-}
\end{pmatrix} = \frac{1}{2} \begin{pmatrix}
1 & \zeta_j^{-1} \\
1 & -\zeta_j
\end{pmatrix}
\begin{pmatrix}
E_{x}(z) \\
H_{y}(z)
\end{pmatrix}
\]  \hspace{1cm} (3b)

By applying eqn (3) through a distinct layer \( j \) of the designed sensor whose thickness is described as, thickness \( d_j = Z_j - Z_1 \), the response of the electric and magnetic fields through the upper and lower surfaces of this layer are given as,
\[
\begin{pmatrix}
E_{x+j} \\
E_{y-j}
\end{pmatrix} = \begin{pmatrix}
\exp[ik_d] & 0 \\
0 & \exp[-ik_d]
\end{pmatrix}
\begin{pmatrix}
E_{x,j+} \\
E_{y,j-}
\end{pmatrix}
\]  \hspace{1cm} (4)

Then, by substituting eqn (4) into eqn (3), we have:
\[
\begin{pmatrix}
E_{x}(z) \\
H_{y}(z)
\end{pmatrix} = \begin{pmatrix}
1 & 1 \\
\zeta_j & -\zeta_j
\end{pmatrix}
\begin{pmatrix}
E_{x+j} \\
E_{y-j}
\end{pmatrix}
\]  \hspace{1cm} (5)

Here, \( W_j \) describes the characteristic matrix of a distinct layer \( j \) that defines the electric and magnetic field components through this layer. Therefore, the matrix that governs the interaction of the electromagnetic waves through the whole designed structure is given as a product of the matrices regarding each constituent layer as:
\[
W = \left( \begin{array}{cc}
W_{11} & W_{12} \\
W_{21} & W_{22}
\end{array} \right) = \prod_{j=1}^{N} W_j = (W_{Ag})(W_{cavity})(W_{GaNCaF2})^N
\]  \hspace{1cm} (6)

Such that, \( W_{11}, W_{12}, W_{21} \) and \( W_{22} \) are the elements of the matrix that governs the interaction between our designed sensor and the incident radiation. This matrix is given as a combination of the matrices of the Ag layer, cavity layer and the periodic structure of \( N \) periods in which each unit cell contains two layers from GaN and CaF\(_2\). Therefore, the structure reflectivity could be described as:
\[
R = \left( \frac{(W_{11}^2 + W_{12}^2 \zeta_{p}) - (W_{21} + W_{22} \zeta_{s})}{(W_{11}^2 + W_{12}^2 \zeta_{p}) + (W_{21} + W_{22} \zeta_{s})} \right)^2
\]  \hspace{1cm} (7)

Here, the two coefficients \( \zeta_{p} = n_p \cos \theta_p \) and \( \zeta_{s} = n_s \cos \theta_s \) stand for the prism as the starting medium and substrate material, respectively. In this regard, the refractive index of the Ag layer can be expressed based on the Drude model such as:
\[
n_{Ag} = \sqrt{1 - \frac{\omega_p^2}{\omega^2 + i\gamma\omega}}
\]  \hspace{1cm} (8)

where \( \omega, \omega_p \) and \( \gamma \) describe the incident frequency, the plasmon frequency of Ag, and the damping constant of Ag, respectively.

On the other side, the fabrication procedure of such a device received a significant contribution. Meanwhile, there are many previous works concerning the fabrication and study of one-dimensional photonic crystal devices. Controlling the thickness of the layers during the fabrication process of the proposed sensor is a very important point for any sensor design. For the fabrication of the design, prism/Ag/cavity/(GaN/CaF\(_2\))\(^{15}\)/air layers, an ultra-smooth Ag layer is deposited on the prism by using the thermal evaporation technique.\(^{24}\) Then, a polyimide polymer film is prepared on the prism/Ag by polymerization of the \( m \)-phenylenediamine monomer. Polyimide has high heat resistance, excellent mechanical properties, and good optical transparency.\(^{25}\) After that, the GaN/CaF\(_2\) multilayer films are deposited on prism/Ag/polyimide. Good crystalline GaN layers can be prepared by using liquid metal gallium surface-nitridation reaction at room temperature.\(^{25}\) High optical quality CaF\(_2\) layers can be grown easily by using magnetron sputtering at low temperatures (<100 °C).\(^{24}\) The whole multilayer structure is now configured as prism/Ag/polyimide/(GaN/CaF\(_2\))\(^{15}\)/air. The polyimide layer can be removed easily by chemical etching.\(^{25}\) Hence, the cavity in a stack of multilayers structure can be carried out for the formation of prism/Ag/cavity/(GaN/CaF\(_2\))\(^{15}\)/air.

3. Numerical verifications and discussions

In this section, we demonstrate the numerical representations that support the dependence on the TP resonance for
a relatively highly-performance sensor for NaI detection. The suggested structure is designed to show the route of the incident electromagnetic waves with wavelengths in the near IR. In the absence of the Ag cavity layer, our design is configured as \{prism/cavity/(Ga\text{N}/Ca\text{F}_2)^{15}/\text{air}\}. Here, the cavity layer with thickness = 5 μm is filled with a water solution. Also, the refractive indices of a prism (SCHOTT), GaN and CaF$_2$ are considered based on the Sellmeier dispersions formula as the following:\textsuperscript{47,56–58}

\[
n_p = \sqrt{1 + \frac{1.55625\lambda^2}{\lambda^2 - 0.0102} + \frac{0.23977\lambda^2}{\lambda^2 - 0.04693} + \frac{0.94789\lambda^2}{\lambda^2 - 69.837}}
\]

\[
n_{CaF_2} = \sqrt{1 + \frac{0.43739\lambda^2}{\lambda^2 - 0.00174} + \frac{0.44921\lambda^2}{\lambda^2 - 0.00783} + \frac{0.15207\lambda^2}{\lambda^2 - 0.01241} + \frac{13.002\lambda^2}{\lambda^2 - 4039.76}}
\]

\[
n_{Ga\text{N}} = \sqrt{3.6 + \frac{1.75\lambda^2}{\lambda^2 - 0.0655} + \frac{4.1\lambda^2}{\lambda^2 - 318.9796}}
\]

In addition, the cavity layer is filled with a water solution. Moreover, the thicknesses of GaN and CaF$_2$ in each unit cell of the one-dimensional PC structure are equivalent to 100 nm and 900 nm, respectively. We can expect from eqn (10) and (11) that there is a relatively high contrast in the refractive indices of CaF$_2$ and GaN materials. This contrast leads to the appearance of a relatively wide PBG through near IR that extends from 1436 nm to 1618 nm with 182 nm in bandwidth for the normal incidence case as shown in Fig. 2. The appearance of this PBG could be of interest in the observation of TP resonance without coupling with other dips. Furthermore, the presence of a cavity layer on the top surface of PCs does not lead to the creation of any defect modes through the PBG. Here, the absence of defect modes could be due to the large thickness of the cavity layer. In particular, the appearance of the defect mode within the PBG is strongly dependent on the quarter-wave stack condition. In another way, the formation of a defect mode through the PBG could be obtained by considering the thickness of the cavity layer in nanometers. However, the choice of this large thickness of the cavity may be preferred from a manufacturing point of view and could lead to more simplicity during the detection as well. Also, the design of the cavity layer as a cap layer on the top surface may represent a second reason.

Then, by including a thin layer of Ag with thicknesses = 30 nm, the final configuration of our design becomes, \{prism/Ag/cavity/(Ga\text{N}/Ca\text{F}_2)^{15}/\text{air}\}. As mentioned before, the refractive index of the Ag layer is investigated based on Drude model for which \(n_{\text{R}}(Ag) = 1.367 \times 10^{16} \text{ rad s}^{-1} \) and \(\gamma(Ag) = 2.73 \times 10^{11} \text{ rad s}^{-1}\). Fig. 3 shows significant changes in the structure reflectivity by including Ag and cavity layers. The figure shows the formation of two reflectance dips in the wavelength’s domain from 1485 nm to 1626 nm. These dips appeared in the vicinity of the PBG due to the TP resonance. The first dip is located at 1485 nm with reflectivity = 22%. Whilst the second one is observed at 1626 nm with reflectivity = 13.4%. The possible quantization of the free electrons at the interface between Ag and cavity layers represents the mainstay of the creation of TP resonance modes.\textsuperscript{60} In other words, the resonant TP dips with low group velocity come as a result of the strong coupling between the evanescent modes present in the periodic dielectric multilayer of the PC and the surface plasmon resonance in the Ag layer.\textsuperscript{61,62} These dips could be of interest through the detection procedure. However, the appearance of only one TP resonance is more preferred than the case of two dips.\textsuperscript{63,64} Usually, the appearance of more than one peak or dip is preferred in applications like filters and multiplexers.\textsuperscript{7,12,15} However, in applications like sensors, it is highly desirable for any design to adjust one peak as an indicator for the input parameter rather

![Fig. 2](image1) The reflectivity of the suggested structure that configured as, \{prism/(Ga\text{N}/Ca\text{F}_2)^{15}/\text{air}\} in the absence of the Ag layer and for the normal incidence case.

![Fig. 3](image2) The reflectance spectrum of the suggested NaI sensor that configured as, \{prism/Ag/cavity/(Ga\text{N}/Ca\text{F}_2)^{15}/\text{air}\} for normal incidence case.
than two or more peaks. In addition, when the spectrum shows two peaks, sometimes this makes a conflict in determining which one is related to the change of the input parameter (like concentration, temperature, etc.). In addition, the appearance of two or more peaks through the spectrum may lead to some conflict, especially with the variation of the analyte concentration. Thus, the coincidence between two different concentrations at the same spectral wavelength due to the presence of two resonant peaks may be present. Moreover, most previous studies of different sensors adopted only one peak to determine the properties of the materials of interest.\textsuperscript{4,11,15}

Therefore, the dependence on the effect of the angle of incidence in producing only one TP resonance mode through the reflectance spectrum could be of potential concern. After the optimization process, we investigated in Fig. 4 the appearance of only one TP resonance mode at an angle of incidence $\theta = 50^\circ$ for TE polarization. The figure clarifies that the produced TP dip is located at 1964 nm with reflectivity $= 0.4\%$. Thus, the oblique incidence for TE polarization with the angle of incidence ($\theta_p$) $= 50^\circ$ reflects the optimum condition in our study. Physically, when the electromagnetic waves interact with our structure at $\theta_p = 50^\circ$, an evanescent mode could be produced due to the penetration of a small portion of the reflected light at the interface between the Ag layer and prism.\textsuperscript{63,64} This evanescent wave comes from the coherent oscillations of free electrons through the Ag layer relative to the alternating electric field of the incident electromagnetic radiation.\textsuperscript{65,66} In particular, the electric field associated with this evanescent wave leads to the excitation of surface plasmon waves at the interface between the cavity and Ag layers. This condition could lead to the creation of a single hybrid Tamm plasmon/surface plasmon resonance mode through the wavelengths of interest. Therefore, this dip represents the core axis during the detection procedure of NaI. Then, to complete the optimization procedure for the most possible high performance, we have discussed in Fig. 5 and 6 the optimum values for Ag and cavity layers. Fig. 5 clarifies the response of the TP resonance modes against the change in the thickness of the Ag layer. Here, the resonant TP dip is shifted downwards the short wavelengths with the increments of Ag layer thickness as shown in the figure. However, the most suitable thickness of the Ag layer that could provide a relatively high performance is investigated at 30 nm. Thus, the optimum value of the Ag layer thickness is 30 nm.

In particular, the metal layer is used to support the surface plasma wave in the proposed structure. The surface plasmon resonance (SPR) can be described as a damped harmonic oscillator (DHO) driven by the electric field component of the incident light. In this context, there are many types of damping may be effective in the SPR mode such as bulk damping and surface damping. The Plasmon-damping rate can be extracted from the resonance linewidth.\textsuperscript{67} The low loss in the energy of plasma waves is desirable for many plasmonic devices such as sensing, imaging, and spectroscopy. Minimizing loss of
plasmonic metal is a critical parameter for strong confinement and thus high-quality SPR. For highly damped plasmons, the plasmon wave may be vanish and the SPR mode is lossy because of the oscillations dying out. The Ag has the lowest bulk-damping coefficient compared with other plasmonic metals in the optical range due to the imaginary component of its dielectric function being very small. The strong coupling of the external optical field with the plasmon wave (photon–electron interaction) suppressed the electron energy loss. Therefore, optimizing the Ag thickness allows the maximum transfer of energy from the light beam to the plasmon wave, which generates the highest coupling between the plasmon wave and the evanescent wave. There is a high oscillating strength of free electrons at the optimum Ag thickness with narrow bandwidth. The reduction of the oscillating strength of plasma electrons due to damping (plasmon decay via coupling with the radiation field) is correlated to the increase of the linewidth of the peak. Hence, the excellent coupling reduces the electron energy loss and the width of the peak due to the effect of damping, which makes the proposed structure more suitable for sensor applications.

Then, to include the optimum thickness of the cavity layer, we replaced the water in the cavity with NaI solution. Meanwhile, the refractive index of NaI solution is fitted based on some experimental data at 23 °C according to the following equation:

\[ n_{\text{NaI}} = 1.335 + 0.09511C + 0.2425C^2 \]  

where \( C \) represents the concentration of NaI through a water solution. Thus, we obtained in Fig. 6 the optimum thickness of the cavity layer relative to the change in the concentration of NaI solution from 0 to 10%. The figure discusses the sensor sensitivity in the form of the shift that occurred for the TP mode with the change in the cavity layer thickness from 3.5 µm to 5.2 µm. At 4.5 µm, a maximum shift of 162 nm in the position of the TP resonance mode is obtained due to the change in NaI concentrations from 0 to 10%. Therefore, the optimum thickness of the cavity layer is considered at 4.5 µm through this study. In this context, we have discussed the performance of our proposed sensor based on this optimum condition in which the angle of incidence = 50° and the thicknesses of Ag and cavity layers are 30 nm and 4.5 µm, respectively.

Now, Fig. 7 reflects the shift in the position of TP resonance mode due to the variations in the concentration of NaI solution from 0 to 25%. The figure shows that the resonant dip is shifted upwards the longer wavelengths with the variation of NaI concentration. As the concentration changes from 0 to 5, 10, and 15%, the reflectance dip is shifted from 1758.1 nm to 1835.5 nm, 1920.8 nm, and 2008.7 nm, respectively. For further increase in NaI concentration to 20 and 25%, the TP resonance is still shifted upwards to 2090.7 nm and 2182.1 nm, respectively. Moreover, the reflectivity of the resonant dip is almost constant, especially at concentrations smaller than 20%. Here, the shift of the resonant dip results due to the change in the optical path length with the increase of NaI concentrations. In this context, at constant thicknesses of the constituent materials and the angle of incidence, the wavelength of the TP resonance mode increases to match the increase in the refractive index of NaI as a result of the increase in its concentration.

This scenario leads to the verification of a constant phase condition (\( \varphi_c = 2\pi nSD\cos(\theta_0)/\lambda \)).

In the midst of the investigated results in Fig. 7, we present in Table 1 the parameters that highlight the performance of the proposed NaI sensor. Table 1 indicates the performance of our sensor in the vicinity of calculating the sensitivity (S), quality factor (QF), detection limit (DL) and figure of merit (FoM). These parameters are calculated based on the following relations:

\[ S = \frac{\Delta \lambda_{TP}}{\Delta C} \]  

\[ QF = S \times DL \]  

\[ FoM = S \times DL \times 10^{-6} \]

![Fig. 7](image_url) The shift in the TP resonance mode relative to the change in the concentration of NaI solution.

### Table 1  
Sensitivity (S), quality factor (QF), detection limit (DL) and figure of merit (FoM) values of the proposed NaI sensor

| C (%) | \( n_{\text{NaI}} \) | \( \lambda_{TP} \) (nm) | Intensity (%) | FWHM (nm) | \( S \) (nm RIU⁻¹) | QF | DL x 10⁻⁶ | FoM |
|------|-----------------|-----------------|-------------|-----------|-----------------|----|-----------|------|
| 0.0  | 1.335           | 1758.10         | 1.35        | 1.04      | —               | 1688.67 | —         | —    |
| 5.0  | 1.3404          | 1836.04         | 0.54        | 1.02      | 14 433.38       | 1787.73 | 3.56      | 14 053.66 |
| 10   | 1.3469          | 1920.79         | 0.09        | 0.99      | 13 672.11       | 1922.89 | 3.65      | 13 687.03 |
| 15   | 1.3547          | 2008.71         | 0.14        | 0.96      | 12 721.56       | 2070.96 | 3.81      | 13 115.83 |
| 20   | 1.3637          | 2090.70         | 1.89        | 0.78      | 11 589.07       | 2661.86 | 3.39      | 14 755.07 |
| 25   | 1.3739          | 2143.72         | 10.51       | 0.31      | 9913.30         | 6902.78 | 1.57      | 31 920.74 |
QF = \frac{\lambda_{TP}}{\text{FWHM}} \quad (13b)

DL = \left( \frac{1}{S} \right) \left( \frac{2(\text{FWHM})^2}{3(\Delta \lambda_{TP})^2} \right) \quad (13c)

\text{FoM} = \frac{S}{\text{FWHM}} \quad (13d)

Such that, \( \lambda_{TP} \) describes the wavelength of the TP resonance mode, \( \Delta \lambda_{TP} \) indicates the shift in the position of TP mode and FWHM describes the full width at the half maximum of the TP resonance mode.

Finally, we have graphically considered the performance of our sensor as indicated in Fig. 8-13 based on the numerical results in Table 1. Fig. 8 shows the change in the position of the TP mode regarding the change in the refractive index of the NaI solution. The figure shows that the position of the resonant TP dip is shifted upwards the longer wavelengths as the refractive index of NaI increases. In general, the resonant TP dip is shifted from 1758.1 nm to 2143.73 nm due to the change in NaI concentration from 0.0 to 25%. This change could be described by the quadratic fitting of the numerical results in Fig. 8 according to the following equation:

\[ \lambda_{TP} = -148038n_{\text{NaI}}^2 + 411024n_{\text{NaI}} - 283123, \quad R^2 = 0.9997 \quad (14) \]

Therefore, at a specified value of \( \lambda_{TP} \), both the refractive index and concentration of NaI could be obtained based on eqn (12) and (14). Then, Fig. 9 describes the sensitivity of our sensing tool versus the variation in the refractive index of NaI. The figure shows that the sensitivity decreases with the increase of the NaI refractive index. However, the value is still exceeding 9913 nm RIU\(^{-1}\). This response could be described in the vicinity of the following fitted equation:

Fig. 8 The position of TP resonance as a function of refractive index for NaI solution.

Fig. 9 The sensitivity of the proposed sensing tool versus the change in the refractive index of NaI solution.

Fig. 10 The change in the values of FWHM of TP resonance with the variations in the refractive index of NaI solution.

Fig. 11 The dependence of QF on the refractive index of NaI solution.
After that, we discussed in Fig. 10 the response of the FWHM of TP resonance versus the change in the refractive index of NaI solution. The figure indicates that the FWHM is slightly decreasing with the increase of the refractive index, especially at $n_{\text{NaI}}$ smaller than 1.3547. Then, a sharp decrease could be investigated at larger values. Here, the decrease in FWHM leads to a sharp profile of the TP resonance mode. In this regard, the plasmon resonance of metal is sensitive to its surrounding environment (local refractive index). Therefore, the damping rate depends on the interface between the Ag layer and NaI solution. This is due to the adsorption of NaI molecules on the Ag surface which affects the polarizability and propagation of the plasmonic wave. This type of damping is called chemical interface damping (CID). The chemical interface damping (CID) refers to the observation that the same Ag layer in

$$S = 2 \times 10^6 (n_{\text{NaI}} - 1) - 944654n_{\text{NaI}}^2, \quad R^2 = 0.999415$$
different chemical environments displays differences in the plasmon line width. Hence, the refractive index of the NaI solution plays an important role in the linewidth of the resonance mode. The NaI solution is polarized in response to the resulting electric field of the plasmon wave. In addition, the polarization of materials is determined by the dielectric function. The imaginary part of the dielectric function for NaI salt is almost zero over the wavelength range 1700–2200 nm and so the NaI solution is considered lossless.

With increasing the refractive index (concentration) of the NaI solution, the permittivity and polarizability of the NaI solution will increase. A material with high permittivity polarizes more in response to an applied electric field than a material with low permittivity, thereby storing more energy in the material. This leads to accelerating the resonance energy transfer from the Ag layer into GaN/CaF₂ multilayer films, and consequently decreasing the loss and lowering FWHM. Thus, the performance of our sensor in the form of the quality factor, detection limit and figure of merit is expected to provide significant improvements.

Then, we plotted in Fig. 11 the dependence of the quality factor on the refractive index of the NaI solution. The figure indicates that the values of QF increase with the increase of the NaI index, especially at $n_{NaI}$ larger than 1.3547. This response could be understood in the vicinity of eqn (13b) and Fig. 10 as a result of the strong dependence of QF on the values of FWHM. Meanwhile, the maximum value of QF (6902) is investigated at $n_{NaI} = 1.3739$ (relative to a concentration of NaI = 25%) in which the smallest value of FWHM is obtained. Moreover, the dependence of QF on the index of NaI according to the fitting of the numerical results as:

$$QF = 2 \times 10^{11} n_{NaI}^5 - 1 \times 10^{12} n_{NaI}^4 + 4 \times 10^{12} n_{NaI}^3 - 5 \times 10^{12} n_{NaI}^2 + 4 \times 10^{12} n_{NaI} - 9 \times 10^{11}, R^2 = 1 \quad (16)$$

Then, Fig. 12 and 13 clarify the response of DL and FoM, respectively against the refractive index of NaI solution. Fig. 12 provides relatively small values of DL that decrease with the increase of the NaI refractive index. In this context, our sensor could receive a DL of 0.157 that supports the efficient performance of this sensor. In addition, the figure of merit increases with the refractive index due to the decrease in the values of FWHM as shown in Fig. 13. Here, our sensor provides a value of FoM over 31 900.

Finally, the investigated results could be of interest towards considering our proposed sensor as a promising platform for NaI detection and sensing. In particular, Table 2 supports this idea compared to its counterparts in optical, photonic and phononic devices. 

4. Conclusions

In this work, we proposed a PC design with the configuration [prism/Ag/cavity/(GaN/CaF₂)]₈/air] as a highly sensitive tool for the detection of NaI solution at different concentrations. Significant changes in the transmission spectra of the proposed structure were produced depending on Ag and cavity layers. The most suitable thickness of the Ag layer that could provide a relatively high performance is investigated at 30 nm. A maximum shift of 162 nm in the position of the TP resonance dip is obtained due to the change in NaI concentration from 0.0 to 10%. As the concentration changes from 0 to 05, 10%, and 0.15, the TP resonance dip is shifted from 1758.1 nm to 1835.5 nm, 1920.8 nm, and 2088.7 nm, respectively. For further increase in NaI concentration to 20 and 25%, the TP resonance dip is still shifted upwards to 2090.7 nm and 2182.1 nm, respectively. The values of QF increase with the increment of NaI refractive index, especially at $n_{NaI}$ larger than 1.3547. The proposed sensor is a promising platform for NaI sensor detector and sensing especially when compared with its counterparts in optical, photonic and phononic devices.

Conflicts of interest

The authors declare they have no conflicts of interests.

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