The scalar and tensor glueball in production and decay

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Abstract

Evidence for the scalar and the tensor glueball is reported. The evidence stems from an analysis of BESIII data on radiative $J/\psi$ data into $\pi^0\pi^0$, $K_SK_S$, $\eta\eta$, and $\phi\omega$ [1]. The coupled-channel analysis is contrained by a large number of further data. The scalar intensity is described by ten scalar isoscalar mesons, covering the range from $f_0(500)$ to $f_0(2330)$. Five resonances are interpreted as mainly-singlet states in SU(3), five as mainly-octet states. The mainly-singlet resonances are produced over the full mass range, the production of octet states is limited to the 1500 to 2100 MeV mass range and shows a large peak. The peak is interpreted as scalar glueball. Its mass, width and yield are determined to $M_{\text{glueball}} = (1865 \pm 25)$ MeV, $\Gamma_{\text{glueball}} = (370 \pm 50^{+30}_{-20})$ MeV, $Y_{J/\psi \rightarrow \gamma G_0} = (5.8 \pm 1.0) \cdot 10^{-3}$. The study of the decays of the scalar mesons identifies significant glueball fractions [2]. The tensor wave shows the $f_2(1270)$ and $f'_2(1525)$ and a small enhancement at $M = 2210 \pm 40$ MeV, $\Gamma = (355^{+60}_{-30})$ MeV [3]. An interpretation of these data is suggested.

1 Introduction

Nearly 50 years ago, Fritzsch and Gell-Mann proposed a new theory of strong interactions: Quantum Chromo Dynamics (QCD) was born [4, 5]. The new theory predicted not only $q\bar{q}$ mesons and $qqq$ baryons but also allowed for the existence of quark-less particles called glueballs. Their existence is a direct consequence of the nonabelian nature of QCD and of confinement. First quantitative estimates of glueball masses were given in a bag model [6]. More reliable are calculations on a lattice where the scalar glueball is predicted to have a mass in the 1500 to 1800 MeV range [7–10]. Analytic approximations to QCD predict the scalar glueball at 1850 to 1980 MeV [11–13]. The tensor glueball is expected to have higher mass, with a mass gap of about 600 MeV. QCD sum rules predict a scalar glueball at about 1780 MeV and
Figure 1: Number of events in the S-wave as functions of the two-meson invariant mass from the reactions $J/\psi \rightarrow \gamma \pi^0\pi^0$ (a), $K_SK_S$ (b), $\eta \eta$ (c), $\phi \omega$ (d). (a) and (b) are based on the analysis of $1.3 \cdot 10^9 J/\psi$ decays, (c) and (d) on $0.225 \cdot 10^9 J/\psi$ decays.

a tensor glueball 100 MeV higher [14]. We thus expect the mass of the scalar glueball to be between 1500 and 2000 MeV and a tensor glueball mass in the 1900 to 2600 MeV range. The mass of the pseudoscalar glueball is expected slightly above the tensor glueball.

Glueballs are embedded into the spectrum of isoscalar mesons. The scalar and tensor glueball have isospin $I = 0$, positive $G$-parity (decaying into an even number of pions), their parity $P$ and their C-parity are positive, and their total spin $J$ is 0 or 2: $(I^G)J^{PC} = (0^+)0^{++}$ or $(0^+)2^{++}$. Glueballs have the same quantum numbers and may mix with them. Most claims for the scalar glueball are based on the observation of three scalar isoscalar resonances, $f_0(1370)$, $f_0(1500)$, and $f_0(1710)$. In this mass range, two isoscalar tensor mesons are known, $f_2(1270)$ and $f_2'(1525)$ where $f_2(1270)$ consists mainly of light quarks ($n\bar{n}$) and $f_2'(1525)$ of strange quarks ($s\bar{s}$). Amsler and Close [15, 16] interpreted these three scalar mesons as mixed states of an $n\bar{n}$, $s\bar{s}$ and the scalar glueball ($gg$). Several authors suggested similar mixing schemes all based on the three resonances $f_0(1370)$, $f_0(1500)$, and $f_0(1710)$ (see [17] and refs. therein).

In this contribution, I present the results on a coupled-channel analysis of BESIII data on radiative $J/\psi$ decays into $\pi^0\pi^0$ [18], $K_SK_S$ [19], $\eta \eta$ [20], and $\omega \phi$ [21]. The results on $J/\psi \rightarrow \gamma 2\pi^+2\pi^-$ [22, 23] and $J/\psi \rightarrow \gamma \omega \omega$ [24] were included in the interpretation of the results. The analysis was constrained by a large number of further data: from the GAMS collaboration on the charge-exchange reactions $\pi^- p \rightarrow \pi^0 \pi^0 n, \eta \eta n$ and $\eta \eta' n$ at 100 GeV/c in a mass range up to 3 GeV, BNL data on $\pi^- p \rightarrow K_SK_S n$, the CERN-Munich data on $\pi\pi \rightarrow \pi\pi$ elastic scattering, the low-mass $\pi\pi$ interactions from the $K_{e4}$ of charged Kaons, and by 15 Dalitz plots on $\bar{p}N$ annihilation. The references to these data can be found elsewhere [1].

2 Radiative $J/\psi$ decays

Radiative $J/\psi$ decays are the prime reaction for searching for glueballs. Lattice gauge calculations predict a branching ratio for radiative $J/\psi$ decays to produce the scalar glueball of $(3.8 \pm 0.9)10^{-3}$ [25] and the tensor glueball with a branching ratio of $(11 \pm 2)10^{-3}$ [26]. This is a significant fraction of all radiative $J/\psi$ decays, (8.8±1.1)%.

The fit to the data – shown in Fig. 1 – requires five pairs of close-by isoscalar resonances.
Table 2 lists the yields of scalar mesons in radiative $J/\psi$ decays in units of $10^{-5}$. RPP numbers are also given for comparison but with two digits only, statistical and systematic uncertainties are added quadratically. The CERN-Munich data on elastic $\pi\pi$ scattering extend up to 1.9 GeV only; the missing intensity can hence be given only up to this mass.

The missing intensity is compared with the $\rho\rho$ and $\omega\omega$ yield in radiative $J/\psi$ decays. The $J/\psi$ yields for $f_0(1750)$ reported in the RPP should be compared to our sum for the yields of $f_0(1710)$ and $f_0(1770)$. The RPP presents yields for $f_0(2100)$ and $f_0(2200)$; they should be compared to the yields of our three high-mass states. The $J/\psi \to \gamma 4\pi$ yield [22, 23] is distributed among these three states.

Figure 3 (left) presents the total yield of H and L scalar mesons in radiative $J/\psi$ decays. Both distributions show a significant yield at about 1900 MeV. The production of mainly-octet scalar mesons is surprising. The production is strong, it could be due to a singlet $q\bar{q}$ component but this hypothesis does not explain the peak structure. We assign the production of high-mass...
Table 2: $J/\psi$ radiative decay rates in $10^{-5}$ units. Small numbers represent the RPP values, except the $4\pi$ decay modes that gives our estimates derived from [22, 23]. The RPP values and those from Refs. [22, 23] are given with small numbers and with two digits only; statistical and systematic errors are added quadratically. The missing intensities in parentheses are our estimates. Ratios for $K\bar{K}$ are calculated from $K_S\bar{K}$ by multiplication with a factor 4. Under $f_0(1750)$ we quote results listed in RPP as decays of $f_0(1710)$, $f_0(1750)$ and $f_0(1800)$. The RPP values should be compared to the sum of our yields for $f_0(1710)$ and $f_0(1770)$. BES [19] uses two scalar resonances, $f_0(1710)$ and $f_0(1790)$ and assigns most of the $K\bar{K}$ intensity to $f_0(1710)$. Likewise, the yield of three states at higher mass should be compared to the RPP values for $f_0(2100)$ or $f_0(2200)$.

| $f_0$ | $\gamma\pi\pi$ | $\gamma K\bar{K}$ | $\gamma\eta\eta'$ | $\gamma\phi\phi'$ | $\gamma\omega\omega$ | missing (total) |
|-------|------------------|------------------|------------------|------------------|------------------|-----------------|
| $f_0(500)$ | $1.3\pm0.2$ | $5\pm1$ | $13\pm4$ | $3.5\pm1$ | $0.9\pm0.3$ | ~0 |
| $f_0(980)$ | $38\pm10$ | $9.0\pm1.7$ | $3.9\pm1.3$ | $2.9\pm1.2$ | $1.7\pm0.5$ | $27\pm1$ |
| $f_0(1370)$ | $3.5\pm1$ | $23\pm8$ | $12\pm4$ | $6.5\pm2.5$ | $1.1\pm0.5$ | $33\pm8$ |
| $f_0(1500)$ | $10.9\pm4.4$ | $24\pm1.2$ | $6.4\pm1.1$ | $4.2\pm0.9$ | $24\pm1.1$ | $36\pm9$ |
| $f_0(1710)$ | $62\pm2$ | $24\pm8$ | $60\pm20$ | $24\pm8$ | $2.5\pm1.1$ | $22\pm4$ |
| $f_0(1770)$ | $99\pm9$ | $59\pm2$ | $95\pm3$ | $24\pm2$ | $25\pm6$ | $97\pm16$ |
| $f_0(2020)$ | $42\pm2$ | $55\pm25$ | $10\pm10$ | $0.7\pm0.5$ | $2.1\pm0.4$ | $115\pm41$ |
| $f_0(2100)$ | $20\pm8$ | $32\pm20$ | $18\pm15$ | $0.7\pm0.5$ | $2.1\pm0.4$ | $115\pm41$ |
| $f_0(2100)/f_0(2200)$ | $5\pm2$ | $5\pm5$ | $0.7\pm0.4$ | $2.1\pm0.4$ | $115\pm41$ | $20\pm3$ |
| $f_0(2200)$ | $62\pm10$ | $109\pm8$ | $110\pm6$ | $4.2\pm0.9$ | $2.5\pm0.5$ | $114\pm21$ |
| $f_0(2330)$ | $4\pm2$ | $2.5\pm0.5$ | $1.5\pm0.4$ | $2.1\pm0.4$ | $115\pm41$ | $20\pm3$ |
scalar mesons to their glueball component. Obviously, H and L scalar mesons have a glueball component of similar strength in their wave function.

To quantify the glueball fractions in the wave functions, we write the wave function of scalar states in the form

\[
f_{0}^{nH}(xxx) = (n\bar{n} \cos \varphi_{n}^{s} - s\bar{s} \sin \varphi_{n}^{s}) \cos \phi_{nH}^{G} + G \sin \phi_{nH}^{G},
\]

\[
f_{0}^{nL}(xxx) = (n\bar{n} \sin \varphi_{n}^{s} + s\bar{s} \cos \varphi_{n}^{s}) \cos \phi_{nL}^{G} + G \sin \phi_{nL}^{G}.
\]

\(\varphi_{n}^{s}\) is the scalar mixing angle, \(\phi_{nH}^{G}\) and \(\phi_{nL}^{G}\) are the meson-glueball mixing angles of the high-mass state H and of the low-mass state L in the nth nonet. The fractional glueball content of a meson is given by \(\sin^{2} \phi_{nH}^{G}\) or \(\sin^{2} \phi_{nL}^{G}\).

The \(q\bar{q}\) component of a scalar meson couples to the final states with the SU(3) structure constant \(\gamma_{a}\) and with a decay coupling constant \(c_{n}\). The structure constants \(\gamma_{a}\) are shown in Fig. 4 as functions of the scalar mixing angle. The SU(3) structure constants \(\gamma_{a}\) of a \(q\bar{q}\) singlet and of a glueball are, of course, identical. There is one coupling constant \(c_{G}\) for the glueball contents of all scalar mesons.

The coupling of a meson in nonet \(n\) to the final state \(\alpha\) can be written as

\[
g_{n}^{\alpha} = c_{n\gamma_{a}} + c_{G\gamma_{a}}^{G}.
\]

The coupling constants were fit to the values derived from the PWA of the BESIII data. Thus, the fractional contributions were determined. The probability that the glueball mixes into one of these resonances is

| Resonance | Fraction (%) |
|-----------|--------------|
| \(f_{0}(1370)\) | (5±4)% |
| \(f_{0}(1500)\) | < 5% |
| \(f_{0}(1710)\) | (12±6)% |
| \(f_{0}(1770)\) | (25±10)% |
| \(f_{0}(2020)\) | (16±9)% |
| \(f_{0}(2100)\) | (17±8)% |

The glueball is distributed, the sum of the fractional contribution is \(78±18\)%

A further contribution (of about 10%) can be expected from the two higher mass states \(f_{0}(2200)\) and \(f_{0}(2330)\). Figure 3 shows the fractional contribution of the scalar mesons to the glueball. The solid curve is a Breit-Wigner function with mass and width \(M = 1865\) MeV, \(\Gamma = 370\) MeV, the area is normalized to one. Obviously, one full glueball is observed.

Further evidence for the glueball nature of the peak in Fig. 3 can be derived from a comparison of \(J/\psi\) radiative decays with the decay \(B_{s} \rightarrow J/\psi f_{0}\). Figure 5 shows the form factor [31] from production of scalar mesons in \(J/\psi \rightarrow \gamma f_{0}\) and \(B_{s} \rightarrow J/\psi f_{0}\) decays [32,33]. The squared form factors are proportional to the yield.

The LHCb data demonstrate that the production of high-mass scalar states is strongly suppressed. The \(f_{0}(980)\) is produced abundantly, there is some \(f_{0}(1500)\) intensity but little production of scalar mesons above this mass. The \(s\bar{s} \rightarrow f_{0}\) yield dies out rapidly with increasing mass. In contrast, two gluons couple strongly to high-mass scalar mesons. The difference is particularly large for the \(f_{0}(1710)/f_{0}(1770)\) resonances in their \(K\bar{K}\) decay. These two resonances decay strongly into \(K\bar{K}\) but are not produced with \(s\bar{s}\) in the initial state, only via two gluons.

### 4 The tensor glueball

With a scalar glueball at 1865 MeV and its large yield in radiative \(J/\psi\) decays we must expect the tensor glueball with an even larger yield. The experimental mass distributions in the \(D\)-wave show large peaks due to \(f_{2}(1270)\) and \(f_{2}(1525)\). In addition, there is a small but wide enhancement at \(M = 2210 ± 40\) MeV, \(\Gamma = (355^{+62}_{-36})\) MeV. This could be the desired tensor glueball. To have the large expected yield, the resonance should have large unobserved decay modes. Certainly, significant more work is required to decide if this is the tensor glueball.
Figure 2: Left: Interference between $f_0(1370)$ and $f_0(1500)$: The BESIII data on $\pi\pi$ and $K\bar{K}$ are shown with the BnGa fit (left) and the JPAC fit (right). In the center, the interference of two Breit-Wigner amplitudes with masses and widths given in Table 1 is shown. A phase difference between the $\pi\pi$ and $K\bar{K}$ decay modes of 180° is required to reproduce the phase difference. One state is singlet in SU(3), the other one octet. Right: Squared masses of mainly-octet and mainly-singlet scalar isoscalar mesons as functions of a consecutive number.

Figure 3: Left: Yield of radiatively produced scalar isoscalar “octet” mesons (open circles) and “singlet” (full squares) mesons. Right: Glueball component in the wave function.

Figure 4: The SU(3) structure constants as functions of the mixing angle $\alpha = \varphi - 90^\circ$. For $\alpha = 0$, the meson is a $n\bar{n}$, for $\alpha = 90^\circ$, it is a $s\bar{s}$ state. Singlet and octet configurations are indicated.
In radiative $J/\psi$ decays mainly-octet and mainly-singlet scalar mesons are produced abundantly. The yield of scalar mesons shows a peak structure; mainly-octet mesons are produced with no background, mainly-singlet mesons above a smooth background. The peak is fit with a Breit-Wigner shape with a pole at $M = (1865 \pm 25) - i(185 \pm 25^{+15}_{-10})$ MeV. The yield is determined to $Y_{J/\psi \rightarrow \gamma G_0} = (5.8 \pm 1.0) \cdot 10^{-3}$. The peak is interpreted as scalar glueball because of the following reasons:

1. Its mass is consistent with QCD predictions.
2. It is produced abundantly in radiative $J/\psi$ decays where glueballs are expected.
3. The yield in radiative $J/\psi$ decays is consistent with QCD predictions.
4. The decay modes of scalar mesons contributing to the glueball yield require a glueball contribution.
5. The glueball fractions of the observed scalar mesons contributing to the glueball add up to $(78 \pm 18)\%$. About 10% are expected from higher-mass states. Hence the full glueball is identified in the decays of scalar mesons.
6. In the reaction $\bar{B}_s \rightarrow J/\psi \rightarrow f_0$ under similar kinematic conditions, scalar mesons of higher mass are only weakly produced. There is little overlap of these scalar mesons with $s\bar{s}$ in the initial state. In radiative $J/\psi$ with two gluons in the initial state, the yield of high-mass scalar mesons is significantly larger: the overlap of these scalar mesons with two gluons is larger.

The search for the tensor glueball in radiative $J/\psi$ decays revealed a several 100 MeV wide peak of little intensity. This could be the tensor glueball but further studies are certainly required to establish its nature.
Figure 6: The scalar and tensor intensities in radiative $J/\psi$ decays to $\pi^0\pi^0$ and $K_SK_S$.

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