Counterbalanced Valve Metal Oxide as a Reliable Dielectric Layer for Electrowetting-on-dielectric Devices

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Valve metal oxide (anodized oxide) is used in a mirrored configuration to serve as self-limiting dielectric layers of electrowetting-on-dielectric (EWOD) devices. Resembling nonpolar electrolytic capacitors, the two opposing metal-dielectric layers always counterbalance each other so that voltages of any polarity can be applied without current flow. By using tantalum pentoxide as the valve metal oxide for experimental evaluation, the mirrored configuration is compared with the usual configuration and further compared with silicon oxide and silicon nitride, which are two dielectric materials commonly used for EWOD. Experiments with a range of applied biases confirm that in a mirrored configuration, one of the two metal-dielectric-electrolyte combinations is always reverse-biased to prevent the current leakage, which is the most common mode of failure for the EWOD devices. The utility is demonstrated by manipulating droplets of KCl solution on both the parallel-plate and one-plate EWOD devices.

1. Introduction

1.1 Dielectric layer for electrowetting

Electrowetting is the apparent phenomenon of contact angle decrease, i.e., wetting, when an electric field is applied between a substrate electrode and an electrically conductive liquid on it, and can actuate the liquid for physical responses.\textsuperscript{(1–4)} To apply a higher voltage for a stronger actuation force without electric current between the liquid and the substrate, a dielectric layer was incorporated between them\textsuperscript{(5)} in a configuration named electrowetting-on-dielectric (EWOD).\textsuperscript{(3)} By arranging electrodes side-by-side, electric potentials can be applied sequentially for basic liquid manipulations, such as droplet generation, movement, splitting, and merging.\textsuperscript{(6)} Because it enables control over the droplet shape and liquid flow using only electrical signals, EWOD actuation has found many applications, including low-
power displays, (1) variable-focus lenses, (7) thermal switches, (8) electrical switches, (9) energy harvesting, (10) and rheometers. (11, 12) As a lab-on-a-chip platform, (13) EWOD has been widely used for applications as diverse as combinatorial synthesis, (14) sample processing, (15, 16) enzyme-linked immunosorbent assay (ELISA), (17) and cell manipulation. (18)

Dielectric properties strongly affect the performance and reliability of EWOD devices. Desired would be a high dielectric constant and a high breakdown strength, so the dielectric could be deposited as a thin layer, which would reduce the voltage that needs to be applied for a given electrowetting effect. (19) It should also be easily deposited as a pinhole-free layer for reliable performance with low fabrication cost. Many dielectrics have been used for EWOD or similar devices [e.g., photoresists, polydimethylsiloxane (PDMS), Parylene, silicon dioxide, silicon nitride, barium strontium titanate (BST), and bismuth zinc niobate (BZT)], (20, 21) but it has been difficult to achieve both high electrical performance and easy deposition, because one generally limits the other.

1.2 Anodic oxide as the dielectric layer for EWOD

Anodic oxides are oxides of valve metals, such as aluminum (Al), bismuth (Bi), tantalum (Ta), and antimony (Sb), and are electrochemically grown by the anodization or anodic oxidation of the metal. These have been extensively used as dielectrics in electrolytic capacitors for their large capacitance owing to their high dielectric constant and large surface area. (22) Recently, these valve metals have been proposed as promising dielectric layers for EWOD owing to their high dielectric constants (8–110), high inherent breakdown strength, and simple low-cost fabrication (low deposition temperature and free of reactive gases). (23–25) Furthermore, grown electrochemically with higher growth rates along weaker insulation paths, the formed layer is considered uniform with few pinholes. (26) However, valve metal oxides are so named because of their current rectifying behavior, which can impose a restricted range of allowable voltages when used for EWOD. (25, 27) Leakage current (cathodic) is almost zero under the anodization bias, but the leakage current (anodic) can become significant under the opposite bias. (26) The current rectifying behavior of the valve metal oxide used for EWOD was demonstrated by Huang et al., (27) who showed that the devices with anodized Ta$_2$O$_5$ performed well when the droplet was applied with a reverse-biased DC or low-frequency voltages under 100 Hz; however, the performance deteriorated severely in the case of forward-biased DC or high-frequency AC voltages.

Despite their current rectifying effect, progress has been made to reliably use valve metal oxides as the primary dielectric in EWOD devices. Huang et al. (27) demonstrated that when Ta$_2$O$_5$ was sputter-deposited (instead of grown electrochemically) onto Ta and then anodized, the final dielectric layer was pinhole-free and insensitive to polarities when tested with 13 V (13% of the anodization formation potential) of actuation, which was sufficient for a contact angle reduction of 18°. It was not tested with higher voltages (greater than 50% of the anodization formation potential), under which a current rectifying effect would be more notable. (26) There is also a concern with the utility of sputtering Ta$_2$O$_5$ before anodizing because an etch process to pattern electrodes would expose Ta sidewalls without the sputtered oxide. In other works,
Dhindsa et al.\(^{(24)}\) demonstrated a reliable EWOD operation within ranges of voltage polarities and droplet compositions, so that any defects in the dielectric would be “self-healed” by further anodization as shown for electrolytic capacitors.\(^{(28)}\)

The rectifying effect of the valve metal oxide was also utilized to create a polarity-dependent EWOD actuation for moving droplets across a surface without the sequential activation of electrodes.\(^{(29,30)}\) The authors used a single high-resistivity electrode and designed exposed aluminum vias through a thermal oxide dielectric, which were spaced so that at least two vias were always beneath the droplet. The native oxide that formed on aluminum (a valve metal) acted as a diode so that current flowed through a via on the low-voltage side but impeded by a via on the high-voltage side of the droplet. The resulting charge accumulation on the high-voltage side caused the droplet to move in its direction. Although current flowed through the droplet, it was limited by the use of diodes with opposite polarities.

1.3 Anodic oxides of mirrored configuration for EWOD

Although electrolytic capacitors use valve metal oxides that have current rectifying effects, nonpolar electrolytic capacitors can be formed when the anodized dielectric is incorporated into both capacitor electrodes in a mirrored (or symmetric) configuration.\(^{(31)}\) In this configuration, one of the two opposing valve metal oxide dielectrics will always be under the reverse bias to restrict current. Following the proposal to adopt the mirrored configuration of nonpolar electrolytic capacitors for the dielectric configuration of EWOD devices and the experimental confirmation using Al as the valve metal in a parallel-plate EWOD device,\(^{(32)}\) in the current report, we adopt Ta as a more suitable valve metal and implement the technology to not only the usual parallel-plate EWOD devices, as illustrated in Fig. 1, but also the coplanar EWOD devices. The valve metal oxides are utilized in such a way that always one is under the reverse bias to limit current. For parallel-plate EWOD devices, the mirrored configuration differs from the typical parallel-plate EWOD, which uses a thinner or no dielectric on one plate. After the basic EWOD characterization of Ta\(_2\)O\(_5\) against silicon oxide and silicon nitride, the mirrored configuration is evaluated against the typical configuration with Ta\(_2\)O\(_5\) as the dielectric. For coplanar EWOD devices, commonly used for single-plate open operations, the mirrored configuration does not differ from the typical. The performance is evaluated by performing the basic EWOD characterization and demonstrating droplet movement.

2. Experimental Procedure

2.1 Anodization

For anodization (or anodic oxidation), the sample valve metal electrode and a counter (unreactive) electrode are immersed in a conducting electrolyte solution, and a bias is applied between the two electrodes (Fig. 2). Oxidation occurs at the anode and reduction occurs at the cathode.\(^{(26)}\) The sample valve metal electrode is connected as the anode (positively charged), where the applied electric field causes oxide growth from both the metal/oxide interface via
Fig. 1. (Color online) EWOD device with a valve metal oxide (e.g., Ta$_2$O$_5$) as the dielectric. (a) The existing configuration is limited by the rectifying behavior. Under reverse (negative) bias, the oxide layer (colored green) blocks current. However, under forward (positive) bias, the oxide layer passes current. Dielectric breakdown is indicated by a white dendrite pattern in the oxide. (b) A mirrored configuration is proposed to ensure that one of the opposing oxide layers is always under reverse bias (the correct bias for this paper) to restrict current and achieve a reliable device.

Fig. 2. (Color online) Anodization setup: platinum was used as a counter electrode and connected to the ground terminal of the power supply. The electrolyte solution was mixed during the process by a magnetic stirrer.
the inward migration of oxygen and the oxide/electrolyte solution interface via the outward migration of metal. Modeled as a linear function of the applied voltage, the oxide thickness from anodization can be precisely controlled by adjusting the applied anodization voltage. However, the anodization constant (or proportionality constant of oxide thickness with respect to voltage) depends on the growth conditions (e.g., electrolyte, concentration, temperature, and pH).

2.2 Sample fabrication

All of the samples were fabricated on clean glass slides (0.7 mm thick) (Fig. 3). For parallel-plate EWOD tests, 500 nm of Ta was sputter-coated on the glass as the EWOD electrodes, on which Ta$_2$O$_5$, silicon nitride, or silicon oxide was formed as the dielectric. Ground plates were also prepared by evaporating 20/200 nm of chrome/gold as the reference electrode for a typical parallel-plate EWOD architecture. A tantalum pentoxide dielectric was grown from sputtered tantalum electrodes by anodization in a room-temperature 0.05 M solution of citric acid in deionized water using a constant current step of 0.1 mA/cm$^2$. The constant current step was followed by a 1-h constant voltage step of 50 V (for 83-nm-thick Ta$_2$O$_5$) or 100 V (for 165-nm-thick Ta$_2$O$_5$). On other samples intended for comparison, silicon oxide and silicon nitride were deposited onto tantalum electrodes at a thickness of 165 nm using PECVD. No dielectric was deposited on the gold-coated ground plates.

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Fig. 3. (Color online) Process flow to fabricate EWOD samples to test and compare a mirrored configuration of valve metal oxide (Ta$_2$O$_5$ shown) as an EWOD dielectric.
For coplanar EWOD tests, two different sets of electrodes were prepared. The first was to actuate sessile droplets to measure the contact angle changes similarly to that described by Yi and Kim,\(^{(35)}\) and the second consisted of two rows of square electrodes to move droplets side-to-side with the sequential activation of neighboring electrodes (Fig. 4). The coplanar EWOD device fabrication began with 500 nm of sputtered tantalum on glass slides. The electrodes were patterned by photolithography with an AZ 4620 photoresist (6.2 µm thick, MicroChemicals GmbH, Germany) and dry-etched by RIE (SF\(_6\) gas, 40 mTorr, 35 V DC bias, and 115 W forward RF power). Before anodization, the photoresist was stripped using a solvent wash and H\(_2\)SO\(_4\)\(\cdot\)H\(_2\)O\(_2\) (4:1) cleaning step. Tantalum pentoxide was anodized under the same conditions as the parallel-plate samples. A hydrophobic layer of Teflon AF 2400\(^{®}\) (35 nm) was spin-coated onto all of the samples and patterned by lift-off to expose the bare metal for electrical contact.

### 2.3 Current leakage and contact angle measurements

In the typical parallel-plate EWOD configuration, a dielectric is used on the main plate with actuation electrodes but not on the ground plate with a reference electrode other than

![Fig. 4](image-url)
the hydrophobic topcoat. In the mirrored configuration for parallel-plate EWOD, both plates include a dielectric (Ta$_2$O$_5$ was used for testing). In the mirrored configuration for coplanar EWOD, Ta$_2$O$_5$ insulated both actuation and reference electrodes on a single plate.

Test droplets consisted of a 1:1 mixture of glycerin and KCl in water standard solution in order to prevent evaporation (with glycerin) and ensure conductivity (with KCl). The chloride from KCl is also useful for testing because it has been shown to exacerbate dielectric failure in EWOD. For parallel-plate current leakage tests, droplets were sandwiched between the plates with a gap of 70 µm. For single-plate actuation tests, sessile droplets were used to measure contact angle changes and demonstrate droplet transportation.

EWOD voltage actuation was supplied by a sourcemeter (Keithley 2425) and leakage current was measured with an electrometer (Keithley 6514). Both Keithley instruments were connected to a computer with a GPIB controller (GPIB-USB-HS, National Instruments) for control and data recording. For cycling tests, mechanical relays (G5LE, OMRON) and photoMOS relays (AQW610EH PhotoMos relay, Panasonic) controlled through a DAQ (NI USB-6255, National Instruments) were used to switch electrical connections to the plates.

Current leakage was measured for both breakdown and lifetime tests. In breakdown tests, currents were measured with respect to the applied electric field. In lifetime tests, current leakage was compared for three types of biases: forward bias, reverse bias, and alternating bias. For all of the biases tested in the lifetime test, 1 s actuation up to 35 V was alternated with 1 s of 0 V, i.e., 0.5 Hz, for 1000 cycles. Contact angles were measured using a contact angle measurement program with images of the droplet during EWOD actuation captured through a CCD camera (PixeLink, model PL B742U).

3. Results and Discussion

3.1 Results for sessile EWOD

The Ta$_2$O$_5$ prepared above was first characterized for its basic performance for EWOD along with two excellent dielectrics (silicon dioxide and silicon nitride), as shown in Fig. 5. In measurements of contact angle change with applied voltage [Fig. 5(a)], an increased actuation was observed with Ta$_2$O$_5$ before contact angle saturation (at ~30 V). The contact angle data is replotted as the electrowetting number $E_w$ in Fig. 5(b) for a better comparison with other EWOD devices in the literature. The above increased actuation compared with those of silicon oxide and silicon nitride at voltages less than 30 V was expected because of the significantly higher dielectric constant of Ta$_2$O$_5$ (21–28) than of silicon oxide (4–6) and silicon nitride (~8). Beyond the saturation voltage, the current leakage of silicon oxide increased significantly compared with those of silicon nitride and Ta$_2$O$_5$ [Fig. 5(c)].

3.2 Results for parallel-plate EWOD

In breakdown tests shown in Fig. 6, the measured leakage currents were low for the Ta$_2$O$_5$ samples, but increased significantly for silicon oxide samples once the voltage increased beyond 5 V or the field beyond 30 MV/m. Silicon nitride samples broke down above 70 V or 425 MV/m.
Fig. 5. (Color online) Basic performance of tantalum pentoxide as the dielectric for EWOD, evaluated with a sessile drop. (a) Contact angle, (b) electrowetting number, and (c) current leakage were measured for three different dielectrics: PECVD silicon nitride (+), PECVD silicon oxide (−), and anodized tantalum pentoxide (○). All of the dielectrics were 165 nm thick. The dimensionless electrowetting number $E_w$ expresses the reduction in the interfacial energy of the solid–liquid interface with the applied electric field.$^{(4)}$ A larger $E_w$ corresponds to a stronger electrowetting effect. Tantalum pentoxide shows a stronger electrowetting effect and a lower current leakage, as long as the reverse bias is maintained, corroborating previous reports.$^{(27)}$

Fig. 6. (Color online) Current leakage measured as a function of electric field across tantalum pentoxide in typical (forward bias, 165 nm; reverse bias, 165 nm) and mirrored (mirrored, 165 nm; mirrored, 330 nm) EWOD devices, tested in parallel-plate configuration. (a) Breakdown voltages of PECVD SiO$_2$ and Si$_3$N$_4$ were measured and overlaid for comparison. (b) Zoomed in for low-leakage data. Tantalum pentoxide dielectrics in the existing configuration under reverse bias and in the mirrored configuration exhibited the lowest current leakage.
Mirrored Ta$_2$O$_5$ samples of the same dielectric thickness broke down at a similar electric field to the silicon nitride, but with a lower current leakage. Current leakage was consistently higher for the forward-biased Ta$_2$O$_5$ than for the reverse-biased Ta$_2$O$_5$. Mirrored configuration samples were made with half the thickness (83 nm) of Ta$_2$O$_5$ on each plate, so that the total dielectric thickness was comparable to that on the test samples (165 nm) used in the typical parallel-plate configuration. In these mirrored configuration samples, the current leakage nearly matched that of the full thickness Ta$_2$O$_5$ samples under reverse bias. The lowest current leakage was measured for Ta$_2$O$_5$ in a mirrored configuration with a full 165 nm thickness on each plate, in which case one half of the externally applied voltage was applied to the 165-nm-thick dielectric.

The cumulative damaging effect of forward bias actuation was clearly seen in lifetime tests with 0.5 Hz of 35 V bias voltage, as shown in Fig. 7. Under forward bias [Fig. 7(a)], the leakage current increased over repeated cycles. The leakage current did not increase steadily because the electrolysis bubbles caused the droplet to shift its position during the measurement. Under reverse bias [Fig. 7(b)], the leakage current was expected to decrease with repeated voltage cycling as a result of self-healing. However, the leakage current was too low for the current instrument to measure a notable decrease. For the mirrored configuration, on the other hand, no significant current change was measured. The test was repeated alternating positive and negative 35 V biases at 0.5 Hz and had similar results. For the single-plate configuration, a significant amount of current leaked during the forward-biased periods of the cycles but not during the reverse-biased periods, as expected. No significant current change was measured for the mirrored configuration.

By using anodized dielectrics in a mirrored configuration, the current leakage was limited during the actuation of a parallel-plate EWOD device, regardless of voltage bias. The fabrication of the mirrored configuration is simpler than adding a sputtering step to deposit a valve metal oxide to address the bias issue. However, its use of an equal dielectric thickness on both plates is somewhat different from that in the case of the typical parallel-plate EWOD devices, which uses the main dielectric only on the plate with patterned EWOD electrodes and leaves the other plate with a much thinner dielectric or just the hydrophobic topcoat.

![Fig. 7.](attachment:image.png) (Color online) Measurement of current leakage under cycles of voltage pulse (0.5 Hz; 50% duty cycle) applied to a droplet on 165-nm-thick tantalum pentoxide in (a,b) typical and (c) mirrored, parallel-plate configurations. (a) The leakage current was significant for forward bias. (b) The leakage current was negligible for reverse bias. (c) For the mirrored configuration, the leakage current was negligible for both biases as well as an alternating bias.
3.3 Results for coplanar EWOD

In the case of coplanar EWOD devices, where both the actuation and reference electrodes are fabricated on the same plate, a mirrored configuration was incorporated with the anodization of only a single plate. Because the valve metal oxide dielectric would still cover both the actuation and ground electrodes, its current rectifying effect should also oppose itself. In this section, the viability of the anodized dielectric in the mirrored configuration is expanded to coplanar actuation, which is the electrode configuration needed for most single-plate EWOD devices.

In sessile droplet actuation with a 5 µL droplet, the current leakage was lower than 15 nA (over a 3 mm² area) for an approximately 20° contact angle change using 25 V, as shown in Fig. 8. In a separate coplanar design with neighboring square electrodes, a 2.5 µL droplet was moved across the electrodes, as shown in Fig. 9, using an actuation voltage of 25 V with an average leakage current of 55 nA during the actuation. The current leakage was somewhat higher for the coplanar EWOD than for the parallel-plate EWOD, considering that 165-nm-thick Ta₂O₅ covered both the actuation and ground electrodes as in the parallel-plate mirrored configuration.

![Fig. 8. (Color online) Basic performance for coplanar EWOD. (a) Contact angle, (b) electrowetting number, and (c) current leakage during EWOD actuation measured on coplanar EWOD electrodes with 165-nm-thick tantalum pentoxide of mirror configuration as the dielectric. Note the unit for current leakage is nA, not µA.](image-url)
with full thickness on both plates. The higher leakage for the coplanar EWOD may be due to
an incomplete insulation along the side edges of tantalum electrodes during the anodization as
the electric field for anodized growth was applied perpendicularly to the surface, while EWOD
actuation involves an electric field parallel to the surface applied along gaps between activated
and grounded electrodes. In such a case, growing more Ta₂O₅ by an additional anodization step
using neighboring electrodes as counter electrodes can improve sidewall insulation.

4. Conclusions

The mirrored configuration for valve metal oxide dielectrics was proposed and verified
using Ta₂O₅ in both parallel-plate and coplanar EWOD devices. In lifetime tests, the mirrored
configuration had negligible current leakage over 1000 actuation cycles. In breakdown tests,
the mirrored configuration did not suffer from the polarity effect, unlike the existing Ta₂O₅
EWOD devices. In comparison with PECVD silicon nitride and silicon oxide, the current
leakage was lower across the Ta₂O₅ dielectrics. Droplet movement was demonstrated on an
open EWOD plate, which has coplanar electrodes covered with Ta₂O₅, while exhibiting little
current leakage as expected from the mirrored configuration.

In this study, we confirmed that valve metal oxides are a viable dielectric material for
EWOD regardless of the bias applied in a mirrored configuration. A simple Ta₂O₅ anodization
process was used for testing, but the dielectric performance may be improved with further
process optimization. Because the conduction mechanism through metal oxides depends on
the conditions in which the oxide is formed and the processing both before and after oxide
growth, additional treatments, such as doping and thermal annealing, may be taken to
improve the dielectric properties.

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References

1. S. Hackwood and G. Beni: Appl. Phys. Lett. 38 (1981) 207.
2. M. G. Pollack, R. B. Fair, and A. D. Shenderov: Appl. Phys. Lett. 77 (2000) 1725.
3. J. Lee, H. Moon, J. Fowler, T. Schoellhammer, and C.-J. Kim: Sens. Actuators, A 95 (2002) 259. https://doi.org/10.1016/S0924-4247(01)00734-8
4. W. C. Nelson and C.-J. Kim: J. Adhes. Sci. Technol. 26 (2012) 1747. https://doi.org/10.1163/156856111X599562
5. B. Berge: Comptes rendus de l’Académie des sciences, Série II 317 (1993) 157.
6. S. K. Cho, Y. Zhao, and C.-J. Kim: Lab Chip 7 (2007) 490. https://doi.org/10.1039/b615665g
7. B. Berge and J. Peseux: Eur. Phys. J. E 3 (2000) 159.
8. G. Cha, C.-J. Kim, and Y. S. Ju: Appl. Therm. Eng. 98 (2016) 189. https://doi.org/10.1016/j.applthermaleng.2015.11.098
9. W. C. Nelson and C.-J. Kim: J. Microelectron. Syst. 18 (2009) 174. https://doi.org/10.1109/JMEMS.2008.2008624
10. T. Krupenkin and J. A. Taylor: Nat. Commun. 2 (2011) 448.
11. B. Berge and J. Peseux: Eur. Phys. J. E 3 (2000) 159.
12. G. Cha, C.-J. Kim, and Y. S. Ju: Appl. Therm. Eng. 98 (2016) 189. https://doi.org/10.1016/j.applthermaleng.2015.11.098
13. B. Berge and J. Peseux: Eur. Phys. J. E 3 (2000) 159.
14. G. Cha, C.-J. Kim, and Y. S. Ju: Appl. Therm. Eng. 98 (2016) 189. https://doi.org/10.1016/j.applthermaleng.2015.11.098
15. P. Sen and C.-J. Kim: J. Microelectron. Syst. 18 (2009) 174. https://doi.org/10.1109/JMEMS.2008.2008624
16. T. Krupenkin and J. A. Taylor: Nat. Commun. 2 (2011) 448.
17. B. Berge and J. Peseux: Eur. Phys. J. E 3 (2000) 159.
18. G. Cha, C.-J. Kim, and Y. S. Ju: Appl. Therm. Eng. 98 (2016) 189. https://doi.org/10.1016/j.applthermaleng.2015.11.098
19. W. C. Nelson and C.-J. Kim: J. Microelectron. Syst. 18 (2009) 174. https://doi.org/10.1109/JMEMS.2008.2008624
20. T. Krupenkin and J. A. Taylor: Nat. Commun. 2 (2011) 448.
21. B. Berge and J. Peseux: Eur. Phys. J. E 3 (2000) 159.
22. G. Cha, C.-J. Kim, and Y. S. Ju: Appl. Therm. Eng. 98 (2016) 189. https://doi.org/10.1016/j.applthermaleng.2015.11.098
23. B. Berge and J. Peseux: Eur. Phys. J. E 3 (2000) 159.
24. G. Cha, C.-J. Kim, and Y. S. Ju: Appl. Therm. Eng. 98 (2016) 189. https://doi.org/10.1016/j.applthermaleng.2015.11.098
25. B. Berge and J. Peseux: Eur. Phys. J. E 3 (2000) 159.
26. G. Cha, C.-J. Kim, and Y. S. Ju: Appl. Therm. Eng. 98 (2016) 189. https://doi.org/10.1016/j.applthermaleng.2015.11.098
27. B. Berge and J. Peseux: Eur. Phys. J. E 3 (2000) 159.
28. G. Cha, C.-J. Kim, and Y. S. Ju: Appl. Therm. Eng. 98 (2016) 189. https://doi.org/10.1016/j.applthermaleng.2015.11.098
29. B. Berge and J. Peseux: Eur. Phys. J. E 3 (2000) 159.
30. G. Cha, C.-J. Kim, and Y. S. Ju: Appl. Therm. Eng. 98 (2016) 189. https://doi.org/10.1016/j.applthermaleng.2015.11.098
31. B. Berge and J. Peseux: Eur. Phys. J. E 3 (2000) 159.
32. G. Cha, C.-J. Kim, and Y. S. Ju: Appl. Therm. Eng. 98 (2016) 189. https://doi.org/10.1016/j.applthermaleng.2015.11.098
33. B. Berge and J. Peseux: Eur. Phys. J. E 3 (2000) 159.
34. G. Cha, C.-J. Kim, and Y. S. Ju: Appl. Therm. Eng. 98 (2016) 189. https://doi.org/10.1016/j.applthermaleng.2015.11.098
35. B. Berge and J. Peseux: Eur. Phys. J. E 3 (2000) 159.
36. G. Cha, C.-J. Kim, and Y. S. Ju: Appl. Therm. Eng. 98 (2016) 189. https://doi.org/10.1016/j.applthermaleng.2015.11.098
37. B. Berge and J. Peseux: Eur. Phys. J. E 3 (2000) 159.
38. G. Cha, C.-J. Kim, and Y. S. Ju: Appl. Therm. Eng. 98 (2016) 189. https://doi.org/10.1016/j.applthermaleng.2015.11.098
39. B. Berge and J. Peseux: Eur. Phys. J. E 3 (2000) 159.