Research Article

Separate Turbo Code and Single Turbo Code Adaptive OFDM Transmissions

Lei Ye¹ and Alister Burr²

¹ Department of Communication Engineering, University of Chongqing, Chongqing 400044, China
² Department of Electronics, University of York, Heslington, York YO10 5DD, UK

Correspondence should be addressed to Lei Ye, yelei0815@gmail.com

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This paper discusses the application of adaptive modulation and adaptive rate turbo coding to orthogonal frequency-division multiplexing (OFDM), to increase throughput on the time and frequency selective channel. The adaptive turbo code scheme is based on a subband adaptive method, and compares two adaptive systems: a conventional approach where a separate turbo code is used for each subband, and a single turbo code adaptive system which uses a single turbo code over all subbands. Five modulation schemes (BPSK, QPSK, 8AMPM, 16QAM, and 64QAM) are employed and turbo code rates considered are 1/2 and 1/3. The performances of both systems with high (10⁻²) and low (10⁻⁴) BER targets are compared. Simulation results for throughput and BER show that the single turbo code adaptive system provides a significant improvement.

1. Introduction

When transmitted in time dispersive channels, the bit error rate (BER) achieved on different orthogonal frequency-division multiplexing (OFDM) subcarriers depends on the frequency domain channel transfer function. The bit errors are normally concentrated in a few severely faded subcarriers in conventional nonadaptive OFDM systems. In the rest of the subcarriers, there are normally no bit errors. If we can identify these high BER subcarriers and apply more powerful, lower rate forward error correction (FEC) codes, the overall BER of the whole OFDM frame will be improved, while employing higher order modulation and higher rate codes on the high-quality subcarriers can improve overall throughput.

Adaptive modulation was proposed for exploiting the time variant Shannonian channel capacity of fading channel by Steele and Webb [1]. In addition to excluding some fading subcarriers and varying the modulation mode, that is adaptive modulation, code rate can also be adapted. Subsequently, Tang [2] contributed an intelligent learning scheme for the appropriate adjustment of switching thresholds. Bizzarri et al. proposed adaptive space-time-frequency coding schemes for multiple-input multiple-output (MIMO) OFDM in [3]. In the present paper, we propose the use of adaptive modulation modes and adaptive code rates for turbo-coded OFDM in two different ways: a single turbo code scheme, and a separate turbo code scheme. In both schemes, each subband [4] contains a set of subcarriers for which the modulation mode and turbo code rate is determined by the signal-to-noise ratio (SNR) of subcarriers in this subband, but in the single turbo code scheme only one turbo code is used over all subbands, while the separate turbo code scheme uses a distinct turbo code frame for each subband.

In the remainder of this paper, we first give a description of the system structure of both adaptive turbo-coded OFDM schemes. We then discuss and compare the numerical results of simulation. The final section gives a summary of the work.

2. System Structure

This adaptive turbo code OFDM system is based on a subband adaptive method. For the separate turbo code adaptive OFDM scheme, the subcarriers are divided into several subbands. Then, the SNR of each subcarrier within the subband is calculated and the modulation mode and code rate for each subband are determined from these SNR values.
Then, separate turbo coding and modulation are employed for each subband. At the transmitter, before adding a cyclic prefix, an inverse fast Fourier transform (IFFT) is applied to the OFDM frames.

After transmission through the fading channel, an FFT is applied to the received signal after removal of the cyclic prefix. Then, each subband is demodulated and decoded separately. The structure of the separate turbo coded adaptive OFDM system used is illustrated in Figure 1.

For the single turbo code adaptive OFDM scheme, the information bits are firstly turbo coded by a single turbo code, then modulated separately for each subband. In the same way, at the receiver, the signal from the output of the FFT is demodulated separately then decoded as a single turbo code frame. In this scheme, when other parameters are the same, the length of turbo code used is much longer than for the separate turbo code scheme, therefore it can get better system performance with the single turbo code adaptive OFDM system. The structure of the single turbo code adaptive OFDM system used is illustrated in Figure 2.

2.1. Transmission Block Structure. In the separate turbo code scheme, the OFDM frame is divided into several subbands, and the turbo code frame combines the same subband of several OFDM symbols. Figure 3 shows the structure of the block and the relationship of turbo code frame and OFDM frame of the separate turbo code scheme.

In the single turbo code scheme, the OFDM frame is also divided into several subbands, each subband using a different modulation scheme. The turbo code frame combines several OFDM symbols. Figure 4 shows the structure of the block and the relationship of turbo code frame, OFDM frame, and cyclic prefix of single turbo code scheme.

Figure 3 shows that the number of modulated symbols in each turbo code frame after coding and modulation should be the same (because the number of subcarriers in each subband is the same). Hence, if different modulation mode and code rate are used for different turbo code frames (different subbands), the length of turbo code must be different for each frame, and therefore the length of the turbo code interleaver must be variable. As shown in Figure 4, the turbo code length of the single turbo code system is also variable because the modulation scheme for the subbands changes. In this work, we choose to use an S-random interleaver for both schemes, which was first described in [5], and hence we need to provide a variable-length S-random interleaver.

Popovski presents a flexible length S-random interleaver algorithm in [6]. In our simulation, we provided a simplified algorithm to generate a flexible S-random interleaver with the same S-parameter as a given interleaver.

Assume that we already have a length $K$ S-random interleaver with S-parameter $S$, denoted by $\pi_K$ and let $L > K$ be the maximal interleaver length of interest. Starting from $N = K$, each permutation $\pi_{N+1}$ of length $K < N + 1 \leq L$ is obtained from the permutation $\pi_N$ by inserting $N$ at position $j_N$ as follows:

$$
\pi_{N+1}(i) = \begin{cases} 
\pi_N(i), & 0 \leq i < j_N, \\
N, & i = j_N, \\
\pi_N(i - 1), & j_N < i \leq N.
\end{cases}
$$

(1)
The length $N + 1$ S-random interleaver is selected using the following steps for given interleaver length $N$ with S-parameter $S$. For each $j_N$ from $0 \rightarrow N$, create an $N + 1$ permutation using (1) above. For each, calculate $D = |\pi_{N+1}(p) - \pi_{N+1}(j_N)|$, for

$$p = \begin{cases} 0 \rightarrow j_N + S, & j_N < S, \\ j_N - S \rightarrow j_N + S, & S \leq j_N < N - S, \\ j_N - S \rightarrow N, & j_N \leq N - S. \end{cases}$$

Then, if $D$ is larger than $S$ for all $p$, this permutation $\pi_{N+1}$ is a length $N + 1$ S-random interleaver with S-parameter $S$. Otherwise, we calculate $D$ for the next permutation $\pi_{N+1}$.

Using this algorithm, all the length $L > K$ S-random interleaver may easily be obtained. Once we find all the positions $j$ for all the lengths of interest, the interleaver can be defined using very simple rules by adding positions to the original length interleaver $\pi_K$ and the values $j_K, j_{K+1}, \ldots, j_{L-1}$.

### 2.2. Adaptation Algorithm for Both Schemes

The adaptation algorithms used for both schemes are the same. Firstly, the
especially when the turbo code length is short. This will affect the adaptive system threshold as well. Figure 5 gives the BER of nonadaptive turbo coded OFDM system.

SNR of each subcarrier needs to be calculated. We assume that the impulse response of the fading channel is time-invariant for the duration of one OFDM symbol. Therefore, the frequency domain channel transfer function $H_n$ can be determined by a Fourier transform of the impulse response. The received data symbols $R_n$ can be expressed as

$$R_n = S_n \cdot H_n + n_n,$$

where $S_n$ is transmission signal and $n_n$ is Gaussian noise. Since the channel's frequency domain transfer function $H_n$ is independent of the noise power in each subcarrier, the local SNR of each subcarrier $n$ can be expressed as

$$\gamma_n = |H_n|^2 \cdot \gamma,$$

where $\gamma$ is the overall SNR. If there is no inter-subcarrier interference (ISI), or interference from other sources, the value $\gamma_n$ determines the bit error probability of subcarrier $n$.

Then, the threshold for the given long-term BER target should be determined. Five modulation schemes, namely, BPSK, QPSK, 8AMPM, 16QAM, and 64QAM are used in these adaptive turbo coded OFDM systems. The turbo code rate is $1/2$. Therefore, there are in total 5 modulation and code schemes for modulation and coding, plus the nontransmission case. By simulating the nonadaptive OFDM system with these schemes separately, the SNR thresholds for a given long-term target BER can be determined. The length of turbo code affects the BER performance of the turbo code especially when the turbo code length is short. This will affect the adaptive system threshold as well. Figure 5 gives the BER curves for each of these schemes with different length of turbo code. Here, we used soft-output demodulation in this system. From this figure, the threshold for the BER target can be determined.

For subband adaptive OFDM transmission, there are several subcarriers with different local SNRs in each subband; therefore the lowest quality subcarrier in the subband is chosen to compare with the threshold, which is fixed threshold adaptation.

In the fixed threshold adaptation, using a conservative approach, the worst subcarrier in each subband is used for channel quality estimation, to determine the modulation mode and the code rate. Therefore, the overall BER in one subband is normally lower than the BER target. If the overall BER can be closer to the BER target (though still below it) by choosing a more suitable modulation mode or code rate, the throughput of the system will be higher. Therefore, we propose an optimal adaptation algorithm giving a better tradeoff between throughput and overall BER by choosing more suitable schemes for each subband on the basis of fixed threshold adaptation.

Firstly, the local SNR for each subcarrier is calculated. Then, the fixed threshold adaptation algorithm should be used to calculate the original scheme $A_n$ for each subband. For each subband, if a higher order scheme $A_n+1$ is employed, the estimated BER of each subcarrier in the subband can be obtained from the BER curve of the nonadaptive system (Figure 5), and hence the estimated average BER of this subband with this scheme $A_n+1$ can be obtained. If the estimated average BER is still lower than the BER target, then we calculate the estimated average BER of this subband with higher order schemes $A_n+2$ and $A_n+3$, and so forth, till the estimated average BER is worse than the BER target. By using this algorithm, the highest order scheme, and therefore the highest throughput, which can fulfil the BER target is found.

3. Numerical Results

3.1. Transmission Assumptions. In the simulation for both systems, we set the BER target to $10^{-2}$. There are 768 subcarriers in each OFDM symbol, which are split into 16 subbands with 48 subcarriers in each. In the separate turbo code adaptive system, for every turbo code frame, subbands from 12 OFDM symbols are combined, which means the length of the signal after turbo encoding and modulation is $48 \times 12 = 576$ modulation symbols. For the single turbo code adaptive system, we still assumed 12 OFDM symbols are combined, and all $768 \times 12 = 9216$ subcarriers are included in one turbo code frame. So, the length of the signal after turbo encoding and modulation is $768 \times 12 = 9216$ modulation
A frequency selective fading channel is assumed in this simulation. The impulse response $h(\tau, t)$ was generated using a tapped delay line channel model in which each tap amplitude follows an independent Rayleigh distribution. The impulse response is shown in Figure 6.

In this simulation, perfect knowledge of the channel transfer function at the receiver is assumed. Also the channel impulse response is not changed during one turbo code frame (12 OFDM symbol) block.

3.2. Simulation Results. In our separate turbo code and single turbo code adaptive turbo-coded OFDM system, as mentioned above, there are five modulation modes with code rate 1/2, plus the nontransmission case. In the separate turbo code system, if one subband is determined to employing BPSK, the length of the turbo code frame used in this subband is 282; while for the subbands employing QPSK, 8AMPM, 16QAM, and 64QAM, the length of the turbo code frames are 570, 858, 1146, and 1722, respectively. Compared to the separate turbo code system, the length of the turbo code in the single turbo code adaptive system is much longer. When none of the subbands are marked as nontransmission, the length of a turbo code with BPSK in all subbands is 4602, and the length of a turbo code with 64QAM in all subbands is 27642.

Figure 7 illustrates the BER performance of both adaptive turbo coded OFDM systems using these 5 modulation schemes, with the optimal adaptation algorithm. Also Figure 8 shows the throughput in bits per second (bps) of both systems using same adaptation algorithm.

The dotted lines in Figure 7 are the BER performances of the nonadaptive OFDM system with 1/2 rate turbo code and the 5 modulation schemes mentioned above. The red solid line with circle in both Figures 7 and 8 are the BER and throughput performance for the separate turbo code system, while the blue solid line with square in both figures is the BER and throughput performance for the single turbo code system. These figures show that the single turbo code adaptive OFDM system can provide better bps throughput performance than the separate turbo code adaptive OFDM system with same adaptation algorithm. Both of the systems fulfil the BER target, but the single turbo code system is closer to it.

3.3. Simulation Results with Rate 1/3 BPSK. As shown in Figure 8, the difference of throughput for these two schemes is smaller when the overall SNR is low. The reason for this is when the SNR is low, there are more subbands with no transmission. So, the length of turbo code in one turbo code system is similar to the length in the separate turbo code system. Hence, a more powerful, lower rate FEC code can be included in the adaptation algorithm to reduce the number of nontransmission subbands. In this case, we choose code rate 1/3 with BPSK as another option.

In the separate turbo code system, it is easy to add a rate 1/3 BPSK scheme. In the single turbo code system, because only one turbo code is used, we initially use the rate 1/3 code. The subbands with code rate 1/2 are achieved by puncturing the parity bit sequences. The process of puncturing is illustrated in Figure 9.
Figure 9: Puncture process of different code rate turbo code ("1" in the table means the code bit is included, "x" means the code bit is punctured).

Figure 10: BER of separate turbo code system and one turbo code system with rate 1/3 BPSK.

Figure 11: Throughput of separate turbo code system and one turbo code system with rate 1/3 BPSK.

Figure 12 illustrates the BER performance of both adaptive turbo coded OFDM systems using these 6 modulation and code schemes, with the optimal adaptation algorithm. Also Figure 11 shows the throughput in bps of both systems using same adaptation algorithm.

The magenta solid lines with cross in both Figures 10 and 11 are the BER and throughput performance for separate turbo code system with code rate 1/3 BPSK, while the black solid lines with star in both figures are the BER and throughput performance for the single turbo code system. The BER performance of both systems is similar to the system without rate 1/3 BPSK, but the throughput performance at lower SNR is slightly higher than the systems without rate 1/3 BPSK.

3.4. Simulation Results for Lower BER Target $10^{-4}$. The advantage of the single turbo coded schemes in the cases simulated here is relatively small because of the relatively high BER target, at which point the required SNR is not much affected by the code length. So, a lower BER target of $10^{-4}$ was chosen for detailed simulation.

Figure 12 illustrates the BER performance of both adaptive turbo-coded OFDM systems with this new BER target. Also Figure 13 shows the throughput in bps of both systems with same BER target. The red solid lines with star in both Figures 12 and 13 are the BER and throughput performance for the separate turbo code system, and the black solid lines with circles in both figures are the BER and throughput...
4. Summary

This paper has presented two adaptive modulations and code rate turbo coded OFDM schemes, namely the separate turbo code system and the single turbo code system, including descriptions of the system structures and transmission signal block structure design. A flexible length S-random interleaver algorithm is used. Also the performances of two adaptive systems have been compared. As shown in the numerical results, for both high and low BER targets, the single turbo code adaptive system provides better performance by using longer turbo codes.

The gap between the turbo-coded systems and the Shannon bound remains large, indicating that substantial further gains should be possible, given that turbo codes are in principle able to approach very closely to this bound. The reasons for the gap here include the rather simple approach to coded modulation for higher order modulation, and that for low code rates the turbo frame (in terms of data bits) is relatively short in both systems. Future work will investigate the use of improved coded modulation and the effect of more realistic channel estimation.

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