Efficient 3D-RSS map estimation method based on area classification

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Abstract: We consider the determination of three-dimensional maps of received signal strength (3D-RSS maps) for disaster-recovery networks enabled by unmanned aerial vehicles (UAVs). In this paper, we extend the existing tensor completion based estimator to propose an efficient new 3D-RSS map estimator. To reduce the sensing route length for the UAV, the proposed method utilizes two approaches for estimating the RSS maps (the tensor completion-based and path-loss-based approaches), depending upon the number of high buildings. We show by simulation experiments that the proposed method can achieve a data-collection time comparable to those of existing methods with a shorter sensing route.

Keywords: received signal strength, tensor completion, unmanned aerial vehicles

Classification: Wireless Communication Technologies

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1 Introduction

Unmanned aerial vehicles (UAVs) are promising for supporting existing terrestrial information networks since they can equipped with wireless communication tools and fly anywhere. In [1], we proposed a message collection and delivery system for UAV-enabled disaster-recovery networks based on three-dimensional maps of received signal strength (3D-RSS maps). The 3D-RSS maps are constructed from sparsely sensed RSS using tensor completion. In [1], we found that RSS maps without any missing stationary points are essential for complete message delivery, while the sensing obviously requires the overhead of measuring many RSSs prior to message delivery. Note that this paper does not target adaptive line-of-sight (LOS) and non-line-of-sight (NLOS) environments selection. Instead, we use RSS maps to determine the UAV locations because previous works have shown that it is difficult to achieve dependable communication by considering either LOS or NLOS links alone. Therefore we use the RSS map derived from the sensed data of the received signals, which include both LOS- and NLOS-related factors.

In this paper, we propose an efficient new 3D-RSS map-estimation method by extending the existing method developed in [1]. Our proposed new method classifies 3D-RSS maps into path loss (PL)-type and tensor completion (TC)-type RSS maps, according to the number of high buildings around the ground stations. We show by simulation experiments that the proposed method can achieve a data-collection time comparable to the existing methods but with a shorter sensing route.

2 System model and assumptions

Figure 1 shows the system model, which involves $P$ stationary transceivers (TRXs), a 3D region over them, and a UAV flying in the region. The region has the size $X \times Y \times Z$ (m$^3$), and it is divided into $N_1 \times N_2 \times N_3 = N_v$ voxels of size $\Delta X \times \Delta Y \times \Delta Z$ (m$^3$). We define the location of the center of gravity of the voxel to be $g_{ijk} = [x_i, y_j, z_k]^\top$, which we refer to as a point. In addition, we define the location of the $q$th TRX to be $t^{(q)} = [t_x^{(q)}, t_y^{(q)}, t_z^{(q)}]^\top$, and we form the set of indexes for all the TRXs: $T = \{1, 2, \ldots, P\}$. The $P$ TRXs transmit their wireless signals to a UAV. To sense the RSS, the UAV visits a number of voxels along a predetermined route $\Omega$.

A 3D-RSS map is defined for each TRX, and a 3D tensor can be defined for the RSS map of the $p$th TRX as follows:

$$t^{(P)} = [t_x^{(p)}, t_y^{(p)}, t_z^{(p)}]^\top$$

Fig. 1. System model.
\[ \hat{R}^{(p)} = \{ R_{ij}^{(p)} \mid 1 \leq i \leq N_1, 1 \leq j \leq N_2, 1 \leq k \leq N_3 \}, \]  

(1)

where \( R_{ij}^{(p)} \) denotes the RSS value at point \( \mathbf{g}_{ijk} \) from the \( p \)th TRX. Note that in \( \hat{R}^{(p)} \), it is not necessary to consider RSS values at voxels far from \( \mathbf{v}^{(p)} \). Therefore, we consider the subset \( \mathcal{R}^{(p)} \subseteq \hat{R}^{(p)} \), which includes only the RSS values at voxels around the given TRX.

### 3 Determination of UAV locations necessary to collect and deliver messages [1]

The UAV locations at which the UAVs need to be positioned to collect and deliver messages, which are hereafter referred to as message points, are determined from the estimated 3D-RSS maps. We define \( \mathbf{w}_q \) \((q = 1, 2, \ldots, Q, Q \leq P)\) as message points.

Let \( \hat{R}^{(p)} \) denote an estimated RSS map of \( \mathcal{R}^{(p)} \). Using the normalized RSS correlation, we decompose \( \mathbf{T} \) into the subsets \( \mathbf{T}_q \), where \( \mathbf{T} = \bigcup_{q=1}^{Q} \mathbf{T}_q \). Defining the RSS value for given \( \mathbf{w}_q \) and \( \mathbf{v}^{(p)} \) as \( R(\mathbf{w}_q, \mathbf{v}^{(p)}) \) (dBm), \( \mathbf{w}_q \) is determined by the following optimization problem:

\[ \max \min_{\mathbf{w}_q, p \in \mathcal{T}_q} R(\mathbf{w}_q, \mathbf{v}^{(p)}). \]  

(2)

Interested readers are referred to [1] for details.

### 4 RSS map-estimation and sensing point determinations

#### 4.1 RSS map-estimation and route establishment

The proposed method estimates the RSS maps using a combination of two different estimators: the PL estimator and the TC estimator. Let

\[ \mathcal{R}^{(all)} = \{ \mathcal{R}^{(p)} \mid p = 1, 2, \ldots, P \} \]  

(3)

denote the set of all the 3D-RSS maps. Each 3D-RSS map is classified into either a PL-type RSS map or a TC-type RSS map based on the area classification described in section 4.2 below. We represent the set of PL-type RSS maps by \( \mathcal{R}_{PL} \subseteq \mathcal{R}^{(all)} \) and the set of TC-type RSS maps by \( \mathcal{R}_{TC} \subseteq \mathcal{R}^{(all)} \).

A PL-type RSS map \( \mathcal{R}_{PL}^{(p)} \) is estimated in [2] using a path-loss model. Let \( \mathbf{g} = [x, y, z]^T \) denote the location of a voxel in \( \mathcal{R}_{PL}^{(p)} \). The PL \( L(p^{(p)}, \mathbf{g}) \) between \( p^{(p)} \) and \( \mathbf{g} \) is given by

\[ L(p^{(p)}, \mathbf{g}) = 22 \log_{10}(d(p^{(p)}, \mathbf{g})) + 28 + 2.0 \log_{10}(f_c), \]  

(4)

where \( d(p^{(p)}, \mathbf{g}) \) denotes the distance between the UAV and the TRX, and \( f_c \) denotes the carrier frequency. The RSS value corresponding to \( \mathbf{g} \) is given by

\[ P_T - L(p^{(p)}, \mathbf{g}), \]  

(5)

where \( P_T \) denotes the transmission power.

On the other hand, in order to estimate the TC-type RSS maps, the UAV visits \( M \) sensing points along route \( \Omega \) and senses RSSs for TRXs at each sensing point. \( \mathcal{R}^{(p)} \) is estimated from the \( M \) RSS values with TC. As in [1], we use the total variation low rank tensor completion method [3]. It is worth mentioning that the length of \( \Omega \) is reduced when more RSS maps are classified as PL-type RSS maps. In this paper, \( \Omega \) is obtained using the genetic algorithm solver in MATLAB [4].
4.2 Area classification
When there are few high buildings around a TRX, the wireless channels between the
TRX and the UAV are very likely to be LOS channels, which means that the 3D-RSS
map for the TRX can be classified as a PL-type RSS map. On the other hand, when
there are high buildings, the 3D-RSS map can be classified as a TC-type RSS map,
because the wireless channels are likely to be NLOS channels.

Therefore, it is reasonable to classify the RSS maps based on the heights of
the surrounding buildings. We define the number of buildings higher than \( \rho_f \) in a
RSS construction area for the \( p \)-th TRX as \( N^{(p)} \). The RSS map \( R^{(p)} \) is classified
as a TC-type RSS map if \( N^{(p)} > N_{th} \), and it is classified as a PL-type RSS map
otherwise, where \( N_{th} \) denotes the threshold value for \( N^{(p)} \).

5 Performance evaluation

To evaluate the performance of the proposed method, we conducted simulation
experiments. Figure 2(a) shows the 3D city map used for the experiments, where
123 TRXs are deployed. Figure 2(b) shows the result obtained by applying the
area classification method described above. We obtained the RSS values by using
the ray-tracing wireless-propagation simulator EEM-RTM [5], which uses the RSS
values as the ground truth for the 3D-RSS maps.

We validated the proposed method, which we term the AC method, by comparing
it with two other methods: the TC method and the PL method. In the TC method,
all the RSS maps are classified as TC-type RSS maps, on the other hand, in the PL
method, they are classified as PL-type RSS maps. Note that the performance of the
TC method is obtained by setting \( \rho_f = 0 \) while that of the PL method is obtained by
setting \( \rho_f = \infty \).

To evaluate the data collection time, we defined the message collection time
between the \( p \)-th TRX and the \( q \)-the message point as

\[
T_c(w_q, t^{(p)}) = \frac{D}{f(R(w_q, t^{(p)}))},
\]

where \( D = 100 \) (MB) denotes the size of the message, and \( f(R(w_q, t^{(p)})) \) (Mbps)
denotes the transmission rate, which is defined as [6]

![Fig. 2. City maps.](image-url)
Figure 3(a) shows the dependence of the AC method on $\rho_f$. The horizontal axis represents the threshold of the number of floors, and the vertical axis is gives the length of the sensing route and the total data-collection time $T_{\text{all}} = \sum_{p=1}^{P} T_c(w_q, t^{(p)})$ for the AC method, normalized by the corresponding values for the TC method. The total length of the sensing route for the AC method decreases as $f$ increases. However, when $\rho_f$ is 11 or higher, the total data-collection time for the AC method becomes infinite, which means that some TRXs have failed to communicate. Because we require 100% coverage of the TRXs, $\rho_f$ must therefore be equal to or less than 10. When $\rho_f = 10$, with only a 12% increase in the data-collection time, the length of the sensing route can be reduced by 60%. Note that the threshold is determined by the environment, and the determination of that quantity will be considered in future work.

Figure 3(b) compares the empirical cumulative distribution function (ECDF) of $T_c(w_q, t^{(p)})$ among the TC, PL, and AC methods, where $\rho_f = 10$. This figure shows that the distribution of the data-collection time for the PL method has a longer tail than for either the AC or TC methods. Eqn. (7) shows that the transmission rate does not increase linearly as the RSS values increase, and by using the RSS map the UAVs can construct an appropriate path by selecting areas that have high RSS values. As a result, the variation of RSS values among the TRXs becomes small, which enables a stable data-transfer rate. On the other hand, the RSS from every TRX may vary randomly in a LOS environment, and the RSS values may be distributed more widely in the PL method, so there can be cases with worse transmission rates. In addition, the ECDF does not converge to 1 in the PL method, which means that some message

\[
f(R(w_q, t^{(p)})) = \begin{cases} 
6.5 & (-82 \leq R(w_q, t^{(p)}) < -79) \\
13.0 & (-79 \leq R(w_q, t^{(p)}) < -77) \\
19.5 & (-77 \leq R(w_q, t^{(p)}) < -74) \\
26.0 & (-74 \leq R(w_q, t^{(p)}) < -70) \\
39.0 & (-70 \leq R(w_q, t^{(p)}) < -66) \\
52.0 & (-66 \leq R(w_q, t^{(p)}) < -65) \\
58.5 & (-65 \leq R(w_q, t^{(p)}) < -64) \\
65.0 & (-64 \leq R(w_q, t^{(p)})) 
\end{cases}
\]
points have infinite data collection times. The reason is that the RSS values are not correctly estimated by using only the PL model.

6 Conclusion

In this paper, we have proposed a new 3D-RSS map-estimation method for disaster recovery networks enabled by UAVs. The method classifies the 3D-RSS maps as TC-type and PL-type RSS maps, depending upon the number of high buildings around the corresponding TRXs. Performance evaluation by simulation experiments showed that the proposed method can reduce the length of the sensing route without increasing the total data collection time.

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