Defining Stress Thresholds of Granite Failure Process Based on Acoustic Emission Activity Parameters

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In order to study the crack closure stress threshold \( \sigma_{cc} \) of hard rock, crack initiation stress threshold \( \sigma_{ci} \), stress threshold \( \sigma_{cs} \) of crack interaction, and damage stress threshold \( \sigma_{cd} \), uniaxial compression test was carried out on granite samples. Stress sensor and dynamic strain gauge are used to measure the load, longitudinal, and lateral deformation of rock in real time. The acoustic emission characteristic parameters of rock fracture process are obtained by using the acoustic emission system. According to the change rule of the AE event rate, cumulative energy, energy rate, duration, and amplitude in the whole process of granite sample fracture, the stress threshold \( \sigma_{cc}, \sigma_{ci}, \sigma_{cs}, \text{ and } \sigma_{cd} \) of each loading stage in the process of rock sample fracture is obtained. The relationship between the stress threshold \( \sigma_{cc}, \sigma_{ci}, \sigma_{cs}, \text{ and } \sigma_{cd} \) of each stage and the uniaxial compressive strength \( \sigma_{UCS} \) of rock samples in the whole process of fracture is analyzed, which shows that the deformation characteristics and crack evolution law of the rock are unified. The research results can provide some reference for further understanding of rock damage evolution mechanism in engineering field.

1. Introduction

The excavation of the tunnel under the deep high ground stress environment breaks the original stress balance state, resulting in local stress concentration, which is very easy to cause rock burst disaster [1]. The safety of human life and property is seriously threatened by rock burst, rock loose, and even roadway instability. Rock burst disaster has become a bottleneck that restricts human beings to seek for mineral resources in the deep. There have been a lot of research studies on the mechanism and prediction of rock burst, but most of them still have some shortcomings. To better understand the mechanism of rock burst, it is necessary to clearly understand the stages of rock fracture. There are a large number of scholars [2–8] at home and abroad, through a variety of means to study the process of rock fracture in detail. It is revealed that the brittle fracture of rock is accompanied by the closure, development, propagation, and interpenetration of internal microcracks. Therefore, the macromechanical properties of rock are closely related to the development of internal microcracks.

Brace et al. [2, 3, 9, 10] have defined five stages of rock failure, as follows: ① crack closure (closing of cracks) deformation \( (0-\sigma_{cc}) \); ② linear elastic deformation \( (\sigma_{cc}-\sigma_{ci}) \); ③ crack (fracture) initiation and stable crack growth \( (\sigma_{ci}-\sigma_{cs}) \); ④ critical energy release and unstable crack growth \( (\sigma_{cs}-\sigma_{cd}) \); and ⑤ failure and postpeak behavior (maximum deformation) \( (\sigma_{uc}-\text{End}) \) based on the stress-strain behavior under compression. Stage ① is the initial loading stage, and the microcracks or micropores in the rock are closed under compressive stress. This stage depends on the distribution and morphology of microcracks in the rock at the initial state. Generally, the axial stress-strain curve in this stage shows strong nonlinear characteristics, and the volume deformation decreases correspondingly, indicating that the rock is in the compression state. Stage ② shows approximate linear elastic characteristics, and axial strain and volume strain are linear. It shows that the microcracks in the rock are closed and still in the compression state. This stage can be used to determine Young’s modulus and Poisson’s ratio of rock. In stage ③, as the axial difference stress continues to
increase, the volume strain curve begins to deviate from the straight line, the volume deformation of rock begins to increase, and the dilatancy phenomenon appears. In stage ⑤, the microcracks in the rock specimen developed and penetrated further, forming visible macrocracks gradually. The axial and lateral strain of the rock specimen continued to increase, and the volume expansion deformation began to accelerate. In the last stage, the accumulated elastic energy in the rock specimen is released, a large number of macrocracks are penetrated, and the rock specimen forms a fracture surface, causing damage. However, Eberhardt et al. [6] believes that the stable crack growth stage \((\sigma_{cs} - \sigma_{cl})\) can be divided into two stages: the stage from the initial crack to crack interaction \((\sigma_{c1} - \sigma_{c2})\) and the stage from the crack interaction to rock failure \((\sigma_{c3} - \sigma_{c4})\). Therefore, according to this viewpoint, the process of rock fracture can be divided into six stages with five thresholds.

The detection of these thresholds, however, has proven difficult especially with respect to crack initiation. A large number of scientific methods have been tried to monitor the process of rock fracture. These techniques involve the use of stress-strain data and acoustic emission monitoring. The process of rock fracture contains abundant acoustic emission information, and the evolution of internal damage is closely related to acoustic emission. AE is directly related to the microfractures in rocks and can be expressed by the damage parameters of rocks. Because the AE signals contain abundant information about crack changes, a number of studies have used AE to investigate the evolution law of crack and rock fracture patterns in Brazilian splitting tests, three-point bending, and compression [11–19]. It is found that there are inevitably subjectivity and uncertainty in the process of determining rock deformation by using the crack volume strain method [20–25]. Thus, if we can identify the relationship between the stress levels and the AE signals in the laboratory or on-site, the damage degree, crack states, and stability of the rock specimen, rock mass, and pillars can be accurately assessed and evaluated. Yang et al. [26] carried out the triaxial compression acoustic emission experiment on limestone, analyzed the damage evolution characteristics of rock under triaxial compression by using the acoustic emission ring count, and established the damage evolution model of rock under triaxial compression based on the cumulative ring count of acoustic emission. Tan et al. [27] simulated the uniaxial compression test of heterogeneous coal-rock assemblage, which obeyed Weibull distribution by particle flow program. The change rule and duration of AE characteristics in different periods are affected by duration. The more inhomogeneous the coal-rock combination body is, the shorter the lasting time in booming period of AE characteristics will be. Zhang et al. [28] discussed the corresponding relationship between the fracture scale and the characteristics of acoustic emission signals and found that the large-scale fracture corresponds to the low frequency and high amplitude acoustic emission signals, while the small-scale fracture corresponds to the low frequency and low amplitude, medium frequency, high frequency, and low amplitude acoustic emission signals.

Based on the corresponding relationship between AE activity and rock damage evolution process, the rock damage state can be quickly understood by AE monitoring technology. In this paper, based on the previous studies, according to the Eberhardt et al. [6] stress threshold division criteria, the acoustic emission technology is applied to the uniaxial compression test of granite samples, to obtain the characteristic parameters of acoustic emission activity in the process of rock deformation and fracture and then to determine the threshold value of each stage of rock loading process before peak pressure. Additionally, the relationship between the thresholds and peaks was analyzed to establish a practical approach toward predicting the rock burst, large deformation of roadways, and rupture of pillars.

2. Experimental Device and Rock Specimens

2.1. Preparation of Specimen. Fifty cylindrical granite specimens were prepared for uniaxial compression testing. The granite specimens were cut and ground into rectangular-shaped specimens with a size of 50 × 50 × 100 mm (length × width × height) and a height to width ratio of 2:1, according to the ISRM recommendations. The surface of both ends of the specimens shall be carefully polished to make the surface flatness within 0.01 mm. The average size and the physical and mechanical parameters of the granite specimens are listed in Table 1.

2.2. Testing System and Apparatus. To test the rock group specimens, we utilized a testing system in the Rock Mechanics Laboratory of Northeastern University. This testing system includes the loading apparatus, recording system of stress-strain data, and a system for AE acquisition and analysis.

1) Loading apparatus and conditions: the loading apparatus used in the experiment was a closed-loop electrohydraulic servo triaxial testing machine, as shown in Figure 1. The main parameters of this loading apparatus are as follows: ① maximum axial force of 3000 kN and the resolution of 20 N; ② the maximum axial deformation of the specimens is 8 mm and the resolution is 0.0005 mm; while the maximum lateral deformation of the specimens is 8 mm and the resolution is 0.0005 mm; ③ the stiffness of the frame was not less than 10 GN/m; and ④ the loading process can be monitored by displacement or force, and the rock specimens used in this experiment were displaced at a speed of 0.06 mm/min.

2) Collection system of data: during the experimental procedure, the force of the loading apparatus and the axial, lateral deformation were measured using the stress sensor and static strain gauges. The resolution of the external displacement sensor is 0.001 mm.

An AE transducer with an operating frequency range of 1 kHz–1 MHz and a nominal resonant frequency of 500 kHz were used in the experiments. The AE system, which is
capable of the two-channel high-speed acquisition and analysis of AE signals, is called Pocket-AE (American Physical Acoustics Company). The AE system discussed below was used to acquire and analyze the signals. During the test, the acoustic emission sensor is closely attached to the specimens, and the contact part between the probe and the specimens is coated with a layer of Vaseline to ensure the coupling effect. To eliminate the end effects and reduce the noise from the pressing system of the loading apparatus, the contact interfaces between the indenter and the testing specimens were evenly coated with butter, and a 3-mm-thick filter plate was attached to both ends of the specimens. The AE monitoring system did not only digitize the signal waveform but also stored the features of each signal. Before testing, it was important to specify particular parameters to ensure the correct recording of the AE data. On the basis of the previous test, the reasonable AE parameters of uniaxial compression test are determined. The sampling frequency is 10 MHz, the gain is 30 dB, the threshold value is 45 dB, the impact definition time is 50 μs, the impact interval time is 300 μs, and the adjusted threshold voltage is 1.0 V.

3. Experimental Results and Discussion

This study carried out analysis to classify the stages of rock deformation and failure defined by Brace et al. [2, 3, 6], based on the characteristics of AE signals under uniaxial compression, such as the rate of AE events, energy, accumulation energy, and AE amplitude. As described previously, in the stable crack development stage, based on the axial and lateral changes of the rock specimens and the AE signal characteristics, we could further classify the stable development stage into two parts: the stage from the initial crack to crack interaction (σci−σci) and the stage from the crack interaction to rock failure (σci−σcd).

3.1. Pre-Existing Crack Closure. Rock is not a homogeneous body, since it contains many gaps such as tiny cracks, lattice gaps, flaws, and other defects. The crack closure threshold (σcc) is defined as the critical value of the rock from a pre-existing crack stage to the linear elastic stage under uniaxial compression. In the stress-strain curve, the critical point prior to the linear elastic deformation is determined by the axial strain changes, from nonlinear to linear behavior. When the primary fracture in the rock sample is closed, the fracture contact surface will occlude, which will cause sporadic acoustic emission phenomenon. Compared with the acoustic emission information in the whole failure of the rock sample, its frequency and energy value are very small. In addition, the cumulative energy of AE is low, but the energy rate hardly fluctuates. These characteristics indicate that the strain energy stored in the rock specimens manifests as elastic waves of small energy during the crack closure process (Figure 2).

Characteristically, as the rate of AE events changes, the energy rate also changes, and the consistency of the AE events and energy release per unit of time become identical. In other words, a dislocation source (for example, crack closure or movement) can cause the displacement of lattices and also trigger an AE event. Additionally, the number of dislocation sources results in the same number of AE events, and the energy released by each AE event at this stage is approximately equal. The three abovementioned factors result in the AE event rate and energy rate being remarkably consistent. At this stage, the amplitude and duration of a single AE event are significantly correlated with the variation of AE event rate (Figures 3 and 4). The duration of AE events was longer at the beginning of loading and then decreased gradually. The amplitude and rate of single AE event decrease with the increase of loading pressure, and the released energy rate is very low in the whole process. Thus, the features with the longer duration and larger amplitude causing the higher rate of AE events in the crack closure stage are in agreement with the general characteristics of the rock specimens because many pre-existing cracks continued to close at lower stress. Because the original rock defects gradually closed with the increase of axial stress, the heterogeneity of the rock specimens eventually decreased to reach the linear elastic phase.

Naturally, the difficulty of using the stress-strain data to identify the crack closure threshold depends on the different rock types. For instance, some brittle rocks are not easy to condense, while, for other rocks, condensation is relatively easy. Therefore, we can use the changes in Young’s modulus...
of the rock during the rock deformation process to determine the crack closure stress threshold. To reduce the error caused by the mutations of the individual point and human subjectivity, we can define the average value of five points around a single point at the threshold of crack closure.

It can be seen from Figures 3–5 that the threshold values are 13.47 MPa and 15.23 MPa, respectively, when using the AE characteristics method and the deformation characteristics approach. The results are slightly different; therefore, we can see that the two methods for determining the crack closure thresholds are similar, although they are based on different concepts. Additionally, crack closure threshold \( \sigma_{cc} \) of the specimen was 14.35 MPa.

3.2. Behavior of Linear Elastic Deformation. When the stress exceeded the crack closure threshold \( \sigma_{ci} \), the rock specimens entered the elastic stage. At this stage, as the axial stress increases, the axial strain stiffness, that is, Young’s modulus, tends to be constant (Figure 5). In Figure 2, we can observe...
various characteristics of the AE signals: lower and smaller AE events; nonincreasing cumulative AE energy; and smaller and more even AE event duration, and lower AE amplitude compared with the crack closure phase (Figures 3 and 4). The differences between the linear elastic deformation and crack closure stages indicate that the rock specimen resembles the linear behavior of elastomer-like springs. The microfractures of the specimens were observed and the number and frequency of the released elastic waves were found to be less and lower, respectively. Thus, the AE signal characteristics can indicate the linear elastic stage. The release of elastic waves during the loading process can be induced by the movement of the crystal lattice and the stress concentration at the crack tips. For the coupling between the event rate and the amplitude of AE signals, both variations with time were reasonably consistent (Figures 3 and 4).

At the late linear elastic stage, the AE event rates sharply increased and the amplitude and duration of the AE signals
increased in a similar manner. These features suggest that the
original defects had been closed in the rock specimens, but
then recovered and entered the initiation stage. Thus,
depending on the changes of AE signal characteristics, we can
determine that the rock specimens reached the stress
threshold of crack initiation. Additionally, the crack initi-
ation stress threshold (σ\textsubscript{ci}) of the specimen was 45.01 MPa.

3.3. Crack Initiation and Development. As the axial load
increased, the cracks constantly initiated, developed, and
ruptured. The stage between the development of the original
independent single crack and the mutual influence of the
adjacent range cracks is called the microcrack stage.

In the initial stage of microcracks, while the values of the
AE event rate and the variation margin were high and large,
respectively, the cumulative energy and energy rate
remained approximately unchanged (Figure 2). This sug-
gests that the number of microcracks was high; however, the
smaller crack volume and lower elastic wave energy stored in
the crack tip means that the rock specimens remained in a
stable phase. From another viewpoint, the AE signal char-
acteristics, such as the short duration and high magnitude of
events can also reflect the crack status and development. At
the stress threshold of crack initiation, the stress-strain curve
slightly deviated from an oblique straight line. However, the
stress continued to increase and the rock specimen surfaces
did not exhibit significant breakdown. These characteristics
imply that the rock was also stable.

In the later stage of crack growth, there are abrupt
cambages in AE event rate, cumulative energy, energy rate,
duration of single AE event, and AE event amplitude
(Figures 2–4). This suggests that the microcracks expanded
from independent development to the interaction of two or
multiple adjacent cracks, and the rock specimens had large
body defects in their interior, which affected their macro-
performance. These weaknesses provided some space for the
penetration of the rupture surface. From the AE charac-
teristic, it can be determined that the stress threshold (σ\textsubscript{ci}) of
the crack interaction for the specimen was 92.58 MPa.

3.4. Interaction of Cracks. The microcracks began to interact
with other cracks, while the AE signals underwent sub-
stantial changes. At this stage, the event rates of the AE
signals and change ranges were much larger compared with
previous stages. Additionally, the accumulated energy rap-
idly increased, and the rate of energy also underwent several
mutations. The subgradient increase of the accumulated
energy indicates that, as brittle as granite is, the instability of
rock rupture was not caused by mutation, but rather by
gradual damage.

There existed an interesting phenomenon whereby the
high rates and the large amplitude of the AE events were
associated with long duration in a certain period. Particu-
larly, the long duration and large amplitude of the AE event
corresponded to low event rates during the occurrence of
large cracks (Figures 3 and 4). The feature of the AE signals
was considered as the basis for determining the occurrence
of large cracks and was termed as the calm stage before rock
fracturing.

3.5. Crack Damage and Critical Energy Release. The accu-
mulated energy during the crack interaction stage under-
went several mutations. Hence, we defined the

3.6. Unstable Development of Cracks and Peak Failure. The unstable development of rock fracture resulted from the
appearance of large cracks in the formation of the final
through-plane. At this stage, the AE characteristics had
unique features: small event rates, high accumulated energy,
big amplitude, and long event duration (Figures 2–4). This
occurred because, when a sizable crack appeared and the
number of large cracks was small, the released energy of
every crack rupture was relatively high. The inflection points
of the stress-strain curve from the point of increase to the
point of decrease is the peak strength. Thus, the peak
strength of the specimen was 105.30 MPa.

3.7. Relationship between Each Threshold and Peak Strength.
According to the abovementioned method, we can use the
characteristics of the AE signals during the axial loading to
determine each stress threshold and calculate the ratio of
each threshold versus the peak strength. Naturally, the stress
threshold can be determined by the observed deformation of
the rock specimens or by carrying out energy calculations.
The results obtained by each of these methods are presented
in Table 2.

For the rock in this experiment, when the load reaches
13% of the peak strength, the rock enters the stage of linear
elasticity, and when the load reaches 55%, the crack begins to
sprout and expand. It should be noted that when the stress is
loaded to 90% of the peak strength, the grains of the rock
specimen will be crushed, the macrocracks will be produced,
and the specimen will move along the fracture surface. This
result proves that the method of acoustic emission is correct
to determine the rock fracture threshold. By comparing the
ratio of stress threshold to peak intensity calculated by
Bieniawski [3] based on the energy accumulation during
uniaxial compression with the ratio of stress threshold to
peak intensity calculated by the acoustic emission charac-
teristic parameters during uniaxial compression, we deter-
mmed that the former was smaller by 10% compared with
the latter. It is believed that this is because granite is a typical
brittle rock and its deformation characteristics are not obvious. Thus, every stress threshold is allowed to be high.

4. Conclusion

This study carried out AE testing by uniaxial compression experiments for a granite group of samples and combined the stress-strain curves and parameters of AE signals in the time dimension. Thus, the stress threshold was determined for each sample throughout the rupture process, and the following conclusions were drawn:

1. In the process of specimen loading, the rate of AE events in the crack growth stage is low, the duration of single AE event is long and the amplitude is large, and the mutation of energy rate occurs. These phenomena can be used as the basis for judging the formation of macrocracks.

2. The crack closure, initiation, development, aggregation, and temporal evolution of rupture under compression are reflected on the information stored in the AE event signals. Therefore, the method based on the AE characteristics is reliable and accurate.

3. Under the action of low stress level, although there are microcracks in the rock, the acoustic emission ring count and energy are relatively small, indicating that the low stress level has little influence on the stability of the rock structure.

4. The stress threshold of each stage of rock fracture can be combined with the acoustic emission monitoring of the engineering site, which provides a reliable basis for the monitoring and prediction of rock burst in the next step.

Data Availability

The data used to support the findings of this study are included within the article.

Conflicts of Interest

The authors declare no conflicts of interest.

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