Effect of Actual Gas Turbine Operating Conditions on Mist/Steam Cooling Performance in a Ribbed Passage

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Abstract: This study numerically examines the effect of actual gas turbine operating conditions on heat transfer characteristics in a ribbed passage with mist/steam cooling. A 60° ribbed passage with aspect ratio of 1/1 was investigated at Reynolds number of 300,000, and steam cooling was used to provide a contrast. Three main factors were considered: coolant temperature, operating pressure, and wall heat flux density. The heat transfer enhancement mechanism of mist/steam cooling was explored, and the results showed that the heat transfer performance of mist/steam cooling was superior to steam cooling. When the coolant temperature varied from 300 to 500 °C, the average Nusselt number of mist/steam cooling decreased by 26.6%, and the heat transfer enhancement ratio dropped from 15% to 10%. As operating pressure increased, the heat transfer performance factor of mist/steam firstly increased and then decreased. At an operating pressure of 1.5 MPa, the heat transfer achieved its optimal performance, and the heat transfer enhancement ratio achieved its maximum value of 15.9%. Larger wall heat flux density provided less heat transfer enhancement. When the heat flux density increased from 100,000 to 300,000 W·m⁻², the average Nusselt number of mist/steam cooling decreased by 13.8%, while the heat transfer enhancement ratio decreased from 25.3% to 12.6%.

Keywords: numerical simulation; internal cooling channel; mist/steam cooling; heat transfer enhancement

1. Introduction

Gas turbines have extensive applications in many important energy production fields, such as aeronautical power, ship propulsion, and power generation. Research has shown that increasing the inlet temperature of the gas turbine is the main approach to enhance its cycle efficiency and output power [1]. With the continuous development of gas turbine technology, the inlet temperature of gas turbines is continuously increasing, exceeding far beyond the allowable temperature for the metal substance of turbine blades. The larger thermal stress caused by the erosion of high-temperature gas not only reduces the mechanical properties of the metal blades but can also easily cause the blade to burn and to be destroyed, which will seriously affect the economy and safety of the gas turbine operation. Therefore, many scholars are devoted to the research on efficient cooling of gas turbine blades.

Back in the 1980s, air was adopted as the coolant for the cooling of gas turbine blades. In the last decades, many researchers have focused on the influence of air cooling technology on the heat transfer performance of gas turbine blades under different structural parameters or various flow conditions [2–5]. However, with the continuous increase in inlet temperature of advanced gas turbines, an increasingly greater amount of cooling air is needed, which will weaken the efficiency of gas turbines.
to a large extent. To solve this problem, steam cooling technology is applied for the cooling of gas turbine blades because steam has better thermophysical properties. Many studies have been carried out on the steam cooling technology for gas turbine blades in order to obtain higher heat transfer performance [6–10]. Although steam cooling of gas turbine blades can decrease air consumption and reduce aerodynamic and thermodynamic loss, a large amount of steam consumption will also lead to many obvious problems, such as low thermal efficiency and more pressure loss, especially in complex ribbed channels. Consequently, one of the challenges for applying traditional air cooling or steam cooling is the low cooling efficiency and large coolant consumption. To meet the requirement of current gas turbines with higher performance, a new cooling technology called the mist/steam two-phase cooling technology has appeared in recent years.

Compared with traditional air cooling and steam cooling, the mist/steam two-phase cooling technology can not only reduce the consumption of coolants but also improve the heat transfer performance of gas turbines. Consequently, it has already attracted a lot of research attention [11–14].

At the beginning of the 21st century, Guo et al. [14–16] experimentally studied the heat transfer performance of mist/steam flow in horizontal straight pipes and 180° bend pipes. They found that the addition of a small amount of droplet could significantly improve the heat transfer enhancement performance. For the horizontal straight pipe, an addition of 5% droplet increased the heat transfer coefficient by 50–100%. For the 180° elbow pipe, an addition of 1–2% droplet increased the heat transfer coefficient by 40–300%. The wall heat transfer coefficient increased with the increase in the steam mass flow rate and decreased with the increase in the wall heat flux density. Subsequently, Dhanasekaran et al. [17,18] conducted a Euler–Lagrange numerical simulation study to verify the heat transfer performance of mist/steam cooling in a horizontal straight pipe and a 180° pipe. The results showed that the maximum numerical prediction error of the steam cooling pipeline was 8%, while that of the mist/steam cooling pipeline was 16%. Elwekeel et al. [19,20] used numerical methods to study the heat transfer performance of square ribs, triangular ribs, and trapezoidal ribs in a 90° transverse ribbed channel. The heat transfer performance of the four coolants—mist/steam, mist/air, steam, and air—were compared, and the results showed that the best heat transfer performance was obtained using mist/steam. In addition, the heat transfer performance of steam could be improved by 130% with the addition of 6% droplets. Liao et al. and Zhang et al. [12,21] adopted a numerical method to compare the heat transfer performance of mist/steam, mist/air, steam, and air in a ribbed wedge-shaped channel and a 45° U-shaped channel. Their results also showed that mist/steam cooling had the best heat transfer performance among the four coolants. Shi et al. [22,23] investigated the effects of Reynolds number, droplet concentration, wall heat flux density, and droplet transport characteristics on the heat transfer performance of mist/steam in a smooth, square passage of turbine blades. Their experiments showed that the heat transfer coefficient of mist/steam was 3.46 times that of pure steam. The heat transfer coefficient of mist/steam increased with the increase of Reynolds number and droplet concentration, while it decreased with the increase in wall heat flux density. Jiang et al. [13] studied the heat transfer characteristics of mist/steam cooling in a 60° ribbed straight channel using both experimental and numerical methods.

The above studies show that mist/steam two-phase flow cooling has good heat transfer enhancement characteristics under the experimental conditions of low temperature, low pressure, low density, and low Reynolds number. However, actual gas turbines work in high temperature, high pressure, and high heat flux density. Such operating conditions not only significantly change the physical properties of steam but also greatly affect the evaporation rate and the dynamic characteristics of droplets. Therefore, the operating conditions of actual gas turbines have a strong influence on the cooling performance of mist/steam two-phase flow. So far, few researchers have studied the cooling characteristics of mist/steam two-phase flow in ribbed channels under the actual operating conditions of gas turbines.

In this work, a numerical study of the effect of high temperature, high pressure, and high heat flux density on the heat transfer characteristics of mist/steam two-phase flow cooling in gas turbine ribbed
channels was carried out in detail using actual operating conditions. The corresponding influence mechanisms of each actual operating condition on the heat transfer enhancement performance of mist/steam cooling were also explored. Furthermore, some quantitative comparisons regarding heat transfer enhancement were conducted between mist/steam cooling and steam cooling. Based on the results, some new conclusions were obtained.

2. Numerical Method

2.1. Geometric Model and Grid Dependency

The dimension of the geometric model adopted in this paper was identical to the experimental research in [24]. A schematic diagram of the computational geometry is shown in Figure 1a, and the numerical calculation model is shown in Figure 1b. The numerical calculation model was mainly composed of an extended inlet section \( L_e \), a ribbed channel section \( L_h \), and an extended outlet section \( L_o \). In order to obtain fully developed flow conditions, the inlet section was extended. Meanwhile, the outlet section was extended to effectively avoid backflow. The detailed parameters were set as follows: channel aspect ratio \( W/H = 1/1; \) section size, \( 40 \times 40 \); rib angle \( \alpha = 60^\circ \); rib height \( \varepsilon = 1.9 \) mm; channel hydraulic diameter \( D = 40 \) mm; rib spacing \( p/\varepsilon = 10 \); length of the heating section of the ribbed channel \( L_h = 400 \) mm; extended inlet section \( L_e = 200 \) mm; extended outlet section \( L_o = 100 \) mm. Symmetric wall boundary conditions were adopted to reduce the computational cost as the geometric model had symmetry in the \( y \)-axis direction.

![Geometric model](image)

(a) Geometric model

![Numerical calculation model](image)

(b) Numerical calculation model

**Figure 1.** Schematic diagram: (a) geometric model and (b) numerical calculation model.

As for the grid meshing, the ANSYS ICEM CFD software was used, and the structured meshing method was adopted. The mesh near the ribbed surface and the smooth surface on both sides were refined, and \( y^+ < 1 \) was guaranteed to meet the requirements of the automatic wall function of the ANSYS CFX solver. The detailed grid meshing of the ribbed channel in the fully developed flow section is shown in Figure 2a. The grid dependency of the geometric model was carried out before the numerical calculation, as shown in Figure 2b. When the number of meshes exceeded 3.23 million, the Nusselt number on the center line of the ribbed surface no longer changed with the increase in the
number of grids. In order to ensure accuracy of the calculation, 4.26 million grids were finally selected for numerical calculation.

![Detailed meshing](image1)

**Figure 2.** Grid characteristics: (a) detailed meshing and (b) grid dependency.

The ANSYS CFX software (14.5, ANSYS, Xi’an, PRC) was used to carry out steady, complicated three-dimensional numerical simulations. The two coolants—mist/steam and steam—were assumed to have constant thermophysical properties. Considering the actual operational condition of gas turbines, compressible and highly turbulent flow were supposed. After review, the shear stress transport (SST) $k$-$\omega$ model, which manages to well predict flow fields, was adopted to obtain the turbulent characteristics. The Euler-Lagrangian particle-tracking method was adopted to numerically simulate mist/steam two-phase flow. The discrete phase adopted the Lagrangian method to capture the motion trajectory of the droplet, and the continuous phase used the Euler method for numerical calculation. The fully coupled bidirectional coupling method was used to consider the interaction between the droplet and the gas flow. Latent heat in phase transition was introduced into the analysis of temperature field during the droplet evaporation process, and the saturation temperature was hypothesized relative to pressure. The governing equations in the domain were solved by the finite volume method. The convection term and diffusion terms were discretized by secondary-order accuracy scheme. The simulations were thought converged when the root mean square (RMS) residuals of the continuous equation, momentum equation, energy equation, and turbulence equation were less than $10^{-5}$. Simultaneously, the average temperature of the ribbed wall, the outlet temperature, and the mass flow rate of the outlet were monitored to ensure that the steady numerical calculation was converged.
2.2. Data Deduction

The inlet Reynolds number ($Re$) of the ribbed channel is defined as follows:

$$Re = \frac{\rho u D}{\mu}$$

where $\rho$ is the coolant density at the inlet; $u$ is the inlet velocity; $D$ is the hydraulic diameter; and $\mu$ is the dynamic viscosity of the coolant.

The friction factor ($f$) is computed as follows:

$$f = \frac{\Delta P}{2 \rho u^2} \frac{D}{L_h}$$

where $\Delta P$ and $L_h$ are pressure and length of heated section, respectively.

Nusselt number ($Nu$) is given by the following equation:

$$Nu = \frac{q}{\left( \frac{T_w}{T_b} \right) \frac{D}{\lambda}}$$

where $q$ is the heat flux density at the surface; $T_w$ and $T_b$ are wall temperature and fluid bulk temperature, respectively; and $\lambda$ is the thermal conductivity of the coolant.

Heat transfer performance factor ($\eta$) is given by the following equation:

$$\eta = \left( \frac{Nu}{Nu_0} \right) / \left( \frac{f}{f_0} \right)^{1/3}$$

where $Nu$ and $f$ are Nusselt number and friction factor, respectively; $Nu_0$ and $f_0$ denote the corresponding values for the plain tube.

2.3. Numerical Method Validation

For the computational domain in Figure 1, the geometric parameters were derived from Shui et al. [24], who experimentally and numerically studied heat transfer characteristics in steam-cooled ducts with 60° rib turbulators. Hence, it was necessary to validate the turbulence model compared with the experimental results. Accordingly, the boundary conditions for validation of the numerical method were set as follows. Steam was selected as the working fluid; the operating pressure and temperature were 0.3 MPa and 447 K, respectively; and heat flux on the heated wall was fixed at 5000 W·m$^{-2}$.

Four turbulence models were compared: standard $k$-$\varepsilon$ model, renormalization group (RNG) $k$-$\varepsilon$ model, standard $k$-$\omega$ model, and SST $k$-$\omega$ model. The boundary conditions were identical to the literature [24]. Figure 3 shows the relationship between the average Nusselt number ($\overline{Nu}$) of the ribbed surface and the Reynolds number ($Re$) in the ribbed straight channels. It can be seen that the standard $k$-$\varepsilon$ model and the RNG $k$-$\varepsilon$ model significantly overestimated $\overline{Nu}$ of all ribbed channels. Within the range of the tested Reynolds number, the predicted values of the standard $k$-$\omega$ model and the SST $k$-$\omega$ model were in good agreement with the experimental values. In contrast, the SST $k$-$\omega$ model had a slightly better prediction than the standard $k$-$\omega$ model, and the maximum error predicted by the SST $k$-$\omega$ model was about 5.76%. Because the standard $k$-$\varepsilon$ model and the RNG $k$-$\varepsilon$ model were not capable enough to accurately predict compressible flow and separation vortices, the corresponding calculation error was larger. On the other hand, the SST $k$-$\omega$ model avoided overestimating eddy viscosity with the consideration of turbulent stress. That made the loss function existing in the energy equation to be closer to the real value. As a result, the prediction error was lower, as shown in Figure 3. Therefore, the SST $k$-$\omega$ model was adopted in this study for subsequent numerical simulations.
As for the numerical validation of mist/steam two-phase flow, the experimental data conducted by Wang et al. [15] to study horizontal straight pipe mist/steam cooling characteristic was used for validation. The geometric model and boundary conditions were also identical to the experimental research [15], and the size of the geometric model is shown in Figure 4a. The heating section was set as the uniform heat flow, and the magnitude was 14,000 W·m⁻². The inlet and outlet extended sections were set as insulated wall. The inlet Reynolds number of pipeline was \( Re = 20,000 \), the inlet steam temperature was 115 °C, and the static pressure in the outlet was 1 atm. As for the discrete phase, the droplet mass fraction was 5.7%, the droplet diameter was 6 \( \mu \)m, and the reflect discrete phase wall boundary condition was adopted. Meshing of the geometric model was conducted in ANSYS ICEM software, and structured grids were adopted. The near-wall grids were refined, as shown in Figure 4b, and \( y^+ < 1 \) was guaranteed. After the grid dependency, the number of grids was finally determined to be 1.43 million.

![Turbulence model validation](image)

**Figure 3.** Turbulence model validation.

![Geometric model and detailed meshing](image)

**Figure 4.** Horizontal smooth circular tube: (a) geometric model and (b) detailed meshing.

Figure 5 shows the distribution of the heat transfer coefficient of the horizontal smooth tube mist/steam cooling wall. The trend of the heat transfer coefficient predicted by numerical simulation was consistent with the experimental data. Except for the area close to the exit area, i.e., in the area close to the exit area, i.e., in the area close to the exit area, i.e., in the area
of \( x/d < 7 \), the predicted value of the wall heat transfer coefficient was in good agreement with the experimental data, and the maximum heat transfer coefficient error was about \( \pm 8.5\% \).

![Figure 5. Distribution of the heat transfer coefficient of the horizontal smooth tube mist/steam cooling wall.](image)

### 2.4. Boundary Conditions

The effect of actual operating conditions of gas turbines, such as inlet temperature (300–500 °C), operating pressure (0.5–5 MPa), and wall heat flux density (100,000–300,000 W·m\(^{-2}\)), on the heat transfer characteristics of mist/steam two-phase flow were studied. The above operating conditions are the actual operating conditions of most ground gas turbines. In order to quantify the mist/steam cooling heat transfer enhancement ratio, steam cooling was selected as a comparative research condition. The mass flow rate in the channel inlet was set according to the Reynolds number, and the inlet temperature of the coolant was also fixed. The inlet turbulence intensity was set as 5%. The reference pressure was given in the calculation domain, and the outlet pressure was set as average static pressure of 0 MPa. The heat flux density was set at the channel ribbed surface and the smooth surfaces on both sides, the symmetry plane was set as symmetrical boundary condition, and the remaining wall surfaces were set as the adiabatic wall surface. All of the wall surfaces were nonslip wall. The droplet mass fraction of the discrete phase was fixed at 5%, the droplet diameter was 20 \( \mu m \), and the discrete phase wall boundary condition was the reflect wall boundary condition. The specific boundary condition parameters are shown in Table 1.

| Variables                                | Numerical Value                  |
|------------------------------------------|----------------------------------|
| Coolant                                  | Mist/steam, steam                |
| Coolant Reynolds number                  | 300,000                          |
| Coolant temperature/°C                   | 300–500                          |
| Operating pressure/MPa                   | 0.5–5                            |
| Heat flux density/W·m\(^{-2}\)           | 100,000–300,000                  |
| Droplet mass fraction                    | 5%                               |
| Droplet diameter/\( \mu m \)             | 20                               |
| Droplet initial temperature/K            | 472                              |
| Droplet initial velocity/m·s\(^{-1}\)   | Same as inlet steam velocity     |
| Discrete phase droplet wall boundary condition | Reflect                     |
3. Discussion of Numerical Results

If there were no extra explanations, the following simulated conditions were set. The steam Reynolds number was fixed as $Re = 300,000$, the coolant temperature was 300 °C, the operating pressure was 1.5 MPa, and the wall heat flux density was 200,000 W·m$^{-2}$.

3.1. Effect of Coolant Temperature

In this study, the coolant temperature range was 300–500 °C. Figure 6 shows the variation in the average Nusselt number ($\overline{Nu}$) of the ribbed surface of mist/steam cooling and steam cooling channels with the coolant temperature. It can be seen that increasing the coolant temperature significantly reduced the heat transfer enhancement capacity of mist/steam cooling. When the steam temperature was increased from 300 to 500 °C, $\overline{Nu}_{\text{mist/steam}}$ decreased by 26.6%, while $\overline{Nu}_{\text{steam}}$ decreased by 23.5%. Compared with the steam cooling channel, the average Nusselt number heat transfer enhancement ratio ($\overline{Nu}_{\text{mist/steam}} / \overline{Nu}_{\text{steam}}$) decreased from 15% to 10%.

Figure 6. Variation in the average Nusselt number of the ribbed surface of mist/steam cooling and steam cooling channels with the coolant temperature.

Figure 7 shows the effect of coolant temperature on the Nusselt number ($Nu$) distribution of the ribbed surface of the mist/steam cooling channel. It can be seen that the $Nu$ distribution in all ribbed channels showed the same trend. As fluid flowed across the ribs, a cobblestone-shaped, high heat transfer region was generated between each rib, and the region grew larger as it came toward the exit. The $Nu$ decreased gradually along the direction of the oblique ribs, while it increased gradually along the flow direction. However, with the increase in the coolant temperature, the $Nu$ in the downstream region of the ribbed channel was significantly reduced.

Figure 8 shows the effect of the coolant temperature on the droplet motion trajectory in the mist/steam cooling channel. It can be seen that, with the increase in the coolant temperature, the running distance of the droplets in the ribbed channel gradually decreased. This was due to the increase in the coolant temperature increasing the evaporation rate of droplets, thereby shortening their lifespan. When the coolant temperature was 300 °C, the droplets could extend the entire ribbed channel heating section. During the evaporation process, droplets strongly mixed with the secondary flow generated in the channel (shown as the variation in the droplet motion trajectory in Figure 8). Consequently, the local heat transfer coefficient increased. When the coolant temperature exceeded 450 °C, droplets completely evaporated before entering the heating section. In contrast to what happened with 300 °C, there was no mixing mechanism between the droplets and the secondary flow. Furthermore, there was no local mainstream temperature decrease caused by the evaporation of droplets. This weakened the heat transfer performance of mist/steam cooling in the ribbed channel. This was also the reason $\overline{Nu}_{\text{mist/steam}} / \overline{Nu}_{\text{steam}}$ gradually decreased with the increase in the coolant temperature, as shown in
Figure 6. The above analysis shows that the droplets that can survive the ribbed channel can enhance the local heat transfer. This is the fundamental reason for the “distributed” cooling characteristic of mist/steam two-phase flow.

![Nusselt number distribution](image)

**Figure 7.** Variation in Nusselt number distribution of the ribbed surface of the mist/steam cooling channel with the coolant temperature.

![Droplet motion trajectory](image)

**Figure 8.** Variation in the droplet motion trajectory of the mist/steam cooling channel with the coolant temperature.

Figure 9 shows the variation in the heat transfer performance factor ($\eta$) of the mist/steam and steam cooling channels with the coolant temperature. It can be seen that the heat transfer performance of the two coolants decreased with the increase in the coolant temperature. $\eta_{\text{mist/steam}}$ was significantly better than $\eta_{\text{steam}}$. When the steam temperature increased from 300 to 500 °C, $\eta_{\text{mist/steam}}$ decreased from 21.7% to 9.7% compared to $\eta_{\text{steam}}$. 
3.2. Effect of Operating Pressure

In this study, the operating pressure range was 0.5–5 MPa. Figure 10 shows the variation in the average Nusselt number \( \overline{Nu} \) of the ribbed surface of mist/steam and steam cooling channels with the operating pressure. It can be seen that \( \overline{Nu}_{\text{mist/steam}} \) increased sharply and then gradually decreased with the increase in the operating pressure. Moreover, \( \overline{Nu}_{\text{mist/steam}} \) peaked when the operating pressure was 1.5 MPa. In contrast, \( \overline{Nu}_{\text{steam}} \) was relatively less affected by the operating pressure. With regard to the average Nusselt number heat transfer enhancement ratio (\( \overline{Nu}_{\text{mist/steam}} / \overline{Nu}_{\text{steam}} \)), it reached a maximum value of 15.9% when the operating pressure was 1.5 MPa. Then, with the increase in operating pressure, \( \overline{Nu}_{\text{mist/steam}} / \overline{Nu}_{\text{steam}} \) gradually decreased to 7.3%.

![Figure 9. Variation in the heat transfer performance factor of the mist/steam and steam cooling ribbed channels with the coolant temperature.](image)

Figure 9. Variation in the heat transfer performance factor of the mist/steam and steam cooling ribbed channels with the coolant temperature.

![Figure 10. Variation in the average Nusselt number of the ribbed surface of mist/steam and steam cooling channels with the operating pressure.](image)

Figure 10. Variation in the average Nusselt number of the ribbed surface of mist/steam and steam cooling channels with the operating pressure.

Figure 11 shows the variation in the Nusselt number (\( Nu \)) distribution of the ribbed surface of the mist/steam cooling channel with the operating pressure. It can be seen that \( Nu \) distributions under different \( P \) conditions were extraordinarily similar. High heat exchange areas gathered close to one side wall of the passage generated between ribs and became bigger along the passage. However, there were still subtle gradations of \( Nu \) on the contours. When the operating pressure was less than 1.5 MPa, \( Nu \) in the downstream area increased with the increase in the operating pressure. When the operating...
pressure exceeded 2.0 MPa, Nu of the ribbed channel surface decreased slightly with the increase in the operating pressure.

![Graph showing variation in Nusselt number distribution](image)

**Figure 11.** Variation in the Nusselt number distribution of the mist/steam cooling channel with the operating pressure.

Figure 12 shows the variation in the droplet motion trajectory of the mist/steam cooling channel with the operating pressure. It can be seen that the operating pressure had a remarkable effect on the droplet motion trajectory. When the operating pressure was less than 1.5 MPa, the droplets could completely survive the entire ribbed channel heating section. In this process, the droplets moved with the mainstream to the downstream of the channel, where droplet evaporation phase transition occurred. Meanwhile, the droplets mixed with the complex secondary flow inside the channel. This significantly enhanced the heat transfer enhancement performance of mist/steam cooling. When the operating pressure was larger than 2.0 MPa, the evaporation rate of the droplets increased, and the running distance of the droplets decreased. The droplets completely evaporated before entering the heating section when the operating pressure exceeded 3.0 MPa. According to the analysis in Section 3.1, the heat transfer enhancement induced by the evaporation of droplets and the mixture with the secondary flow no longer existed, so the heat transfer enhancement performance of mist/steam cooling was weakened.

Figure 13 shows the variation in the heat transfer performance factor ($\eta$) of the mist/steam and steam cooling channels with the operating pressure. It can be seen that $\eta_{\text{mist/steam}}$ first increased and then decreased with the increase in the operating pressure, and it peaked when the operating pressure was 1.5 MPa. However, the variation in $\eta_{\text{steam}}$ was not obvious with the increase in the operating pressure. When the operating pressure was 1.5 MPa, $\eta_{\text{mist/steam}}$ was 21.7% higher than $\eta_{\text{steam}}$. 
3.3. Effect of Heat Flux Density

In this study, the wall heat flux density range was 100,000–300,000 W·m\(^{-2}\). Figure 14 plots the variation in the average Nusselt number (\(\overline{Nu}\)) of the ribbed surface of mist/steam and steam cooling channels with the wall heat flux density. It can be seen that both \(Nu_{\text{mist/steam}}\) and \(Nu_{\text{steam}}\) declined as the wall heat flux density increased. In the range of heat flux density investigated in this study, the decrease in \(\overline{Nu}_{\text{mist/steam}}\) and \(\overline{Nu}_{\text{steam}}\) reached 13.8% and 4.1%, respectively. The heat transfer enhancement ratio (\(\overline{Nu}_{\text{mist/steam}} / \overline{Nu}_{\text{steam}}\)) decreased from 25.3% to 12.6%.

Figure 15 shows the distribution of the mist/steam cooling passage with different wall heat flux densities. It can be seen that the \(Nu\) distribution characteristics of the high heat transfer regions were similar to the previous cases. The regions produced between ribs almost covered the whole
downstream area of the ribbed surface, and the \( Nu \) presented a decreasing trend with the increase in wall heat flux on the surface.

![Figure 14](image1.png)

**Figure 14.** Variation in the average Nusselt number of the ribbed surface of mist/steam and steam cooling channels with the wall heat flux density.

![Figure 15](image2.png)

**Figure 15.** Variation in the Nusselt number distribution of the mist/steam cooling channel with the wall heat flux density.

Figure 16 presents the effect of the wall heat flux density on the droplet trajectories in the mist/steam cooling passage. From Figure 16a, it can be seen that the impact of \( q \) was quite limited. The trajectories were mainly affected by the secondary flow generated in the passage. Figure 16b plots the trajectories as viewed from the right side. It shows that the droplets spun around clockwise under the force of the main flow and the secondary flow. The droplet trajectories in the mainstream core region were hardly changed under various wall heat flux densities. However, the liquid drops near the ribbed surface traveled farther when the wall heat flux density declined. Due to the strong mixture between droplets and the main flow and secondary flow, heat and mass transfer were enhanced in the mainstream core region. When the droplets moved toward the heated wall, affected by the high heat flux, the
evaporation rate increased rapidly. Due to this, the trajectories near the wall were shortened, while those in the mainstream were seldom impacted. For steam cooling, increasing heat flux lifted the fluid temperature near the wall, which reduced the temperature gradient of the thermal boundary layer. Hence, heat transfer was weakened. For mist/steam cooling, higher heat flux resulted in droplets failing to intrude into the region near the heated wall. The disturbance to the thermal boundary and the interaction between the droplets and the wall were both weakened. This explains why higher \( q \) provided lower heat transfer for mist/steam cooling.

Figure 17 shows the variations in \( \eta \) in the mist/steam and steam cooling passages with the wall heat flux density. For both coolants, \( \eta \) decreased as the wall heat flux density increased, with \( \eta \) in mist/steam cooling declining more quickly. For instance, when the wall heat flux density rose from 100,000 to 300,000 W·m\(^{-2}\), \( \eta \) in the mist/steam cooling passage decreased by 16.5%, while that of steam cooling decreased by 6.9%.

![Figure 16. Variation in the droplet motion trajectory of the mist/steam cooling channel with the wall heat flux density.](image16)

![Figure 17. Variation in the heat transfer performance factor of the mist/steam and steam cooling channels with the wall heat flux density.](image17)
4. Conclusions

This study examined the heat transfer characteristics in a ribbed passage with mist/steam cooling under actual gas turbine operating conditions. The effects of the coolant temperature, the operating pressure, and the wall heat flux density were investigated. The influence mechanism of the operating conditions on the heat transfer enhancement performance of mist/steam cooling was also analyzed. The main conclusions are as follows:

(1) Mist/steam cooling could enhance heat transfer in the ribbed passage under all working conditions used in this study, in contrast to steam cooling.

(2) The average Nusselt number on the ribbed surface and the heat transfer performance factor decreased with the increase in the coolant temperature in both mist/steam cooling and steam cooling passages. However, the cooling performance of mist/steam was more sensitive to the coolant temperature. With the increase in the coolant temperature, the heat transfer enhancement ratio of mist/steam cooling in heat transfer decreased gradually. For mist/steam cooling, the average Nusselt number decreased by 26.6%, and the heat transfer enhancement ratio decreased from 15% to 10% when the coolant temperature varied from 300 to 500 °C.

(3) The average Nusselt number and the heat transfer performance factor first increased and then decreased with the increase in the operating pressure, reaching the peak at the pressure of 1.5 MPa. Under that pressure, the heat transfer enhancement ratio of mist/steam cooling was enhanced by 15.9% compared with steam cooling.

(4) The heat transfer performance factor was greatly reduced with the increase in wall heat flux density. As the wall heat flux density rose from 100,000 to 300,000 W·m⁻², the average Nusselt number of mist/steam cooling decreased by 13.8%. In the meantime, the heat transfer enhancement ratio of mist/steam cooling to steam cooling decreased from 25.3% to 12.6%.

(5) Under actual operating conditions of gas turbines, it is recommended that higher steam Reynolds number (Re = 300,000), lower steam temperature (300 °C), medium operating pressure (1.5 MPa), and lower wall heat flux density (100,000 W·m⁻²) be used to obtain the optimal heat transfer enhancement performance of mist/steam cooling.

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**Nomenclature**

\[D\] Hydraulic diameter of channel, mm  
\[e\] Rib eight, mm  
\[f\] Friction factor  
\[H\] Height of channel, mm  
\[L\] Length, mm  
\[Nu\] Nusselt number  
\[\overline{Nu}\] Average Nusselt number  
\[p\] Rib pitch, mm  
\[P\] Operating pressure, MPa  
\[\Delta P\] Pressure drop of heated section, Pa  
\[q\] Wall heat flux density, W/m²  
\[Re\] Reynolds number  
\[T\] Coolant temperature, °C  
\[u\] Inlet velocity, m·s⁻¹  
\[W\] Width of channel, mm
Greek symbols
- \( \alpha \): Rib angle, \(^\circ\)
- \( \rho \): Density of the coolant, \( \text{kg} \cdot \text{m}^{-3} \)
- \( \mu \): Dynamic viscosity of the coolant, \( \text{Pa} \cdot \text{s} \)
- \( \lambda \): Fluid thermal conductivity, \( \text{W} \cdot \text{m}^{-1} \cdot \text{K}^{-1} \)
- \( \eta \): Heat transfer performance factor.

Subscript
- 0: A plain tube
- e: Extended entrance section
- h: Heated section
- o: Extended outlet section
- mist: Mist/steam cooling
- steam: Steam cooling
- w: Wall
- b: Fluid bulk

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