Discovering Dialog Structure Graph for Coherent Dialog Generation

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Abstract
Learning discrete dialog structure graph from human-human dialogs yields basic insights into the structure of conversation, and also provides background knowledge to facilitate dialog generation. However, this problem is less studied in open-domain dialogue. In this paper, we conduct unsupervised discovery of discrete dialog structure from chitchat corpora, and then leverage it to facilitate coherent dialog generation in downstream systems. To this end, we present an unsupervised model, Discrete Variational Auto-Encoder with Graph Neural Network (DVAE-GNN), to discover discrete hierarchical latent dialog states (at the level of both session and utterance) and their transitions from corpus as a dialog structure graph. Then we leverage it as background knowledge to facilitate dialog management in a RL based dialog system. Experimental results on two benchmark corpora confirm that DVAE-GNN can discover meaningful dialog structure graph, and the use of dialog structure as background knowledge can significantly improve multi-turn coherence.

1 Introduction
With the aim of building a machine to converse with humans naturally, some work investigate neural generative models (Shang et al., 2015; Serban et al., 2017). While these models can generate locally relevant dialogs, they struggle to organize individual utterances into globally coherent flow (Yu et al., 2016; Xu et al., 2020b). The possible reason is that it is difficult to control the overall dialog flow without background knowledge about dialog structure. However, due to the complexity of open-domain conversation, it is laborious and costly to annotate dialog structure manually. Therefore, it is of great importance to discover open-domain dialog structure from corpus in an unsupervised way for coherent dialog generation.

Some studies tried to discover dialog structure from task-oriented dialogs (Shi et al., 2019). However, the number of their dialog states is limited to only dozens or hundreds, which cannot cover fine-grained semantics in open-domain dialogs. Furthermore, the dialog structures they discovered generally only contain utterance-level semantics (non-hierarchical), without session-level semantics (chatting topics) that are essential in open-domain dialogs (Wu et al., 2019; Kang et al., 2019; Xu et al., 2020c). Thus, in order to provide a full picture of open-domain dialog structure, it is desirable to discover a two-layer directed graph that contains session-level semantics in the upper-layer vertices, utterance-level semantics in the lower-layer vertices, and edges among these vertices.

In this paper, we propose a novel discrete variational auto-encoder with graph neural network (DVAE-GNN) to discover a two-layer dialog structure from chitchat corpus. Intuitively, since discrete dialog states are easier to capture transitions for dialog coherence, we use discrete variables to represent dialog states (or vertices in the graph) rather than dense continuous ones in most VAE-based dialog models (Serban et al., 2017; Zhao et al., 2017). Specifically, we employ an RNN Encoder with softmax function as vertex recognition module in DVAE, and an RNN decoder as reconstruction module in DVAE, as shown in Figure 3. Furthermore, we integrate GNN into DVAE to model complex relations among discrete variables for more effective discovery. The parameters of DVAE-GNN can be optimized by minimizing a reconstruction loss, without the requirement of any annotated datasets.

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1Dialog structure means dialog states and their transitions.
2A session refers to a dialog fragment about one topic.]
As shown in Figure 1, with well-trained DVAE-GNN, we build the dialog structure graph by three steps. **First**, we map all dialog sessions to utterance-level and session-level vertices, as shown in Figure 1 (b); **Second**, we calculate co-occurrence statistics of mapped vertices for all dialog sessions, as shown in Figure 1 (c).³ **Finally**, we build edges among vertices based on all collected co-occurrence statistics to form the dialog structure graph, as shown in Figure 1 (d).

To prove the effectiveness of the discovered structure, we propose a hierarchical reinforcement learning (RL) based graph grounded conversational system (GCS) to leverage it for conversation generation. As shown in Figure 2, given a dialog context, GCS first maps it to a utterance-level vertex, and then learns to walk over graph edges, and finally selects a contextual appropriate utterance-level vertex to guide response generation at each turn.

Our contribution includes: (1) we identify the task of unsupervised dialog structure graph discovery in open-domain dialogs. (2) we propose a novel model, DVAE-GNN, for hierarchical dialog structure graph discovery. Experimental results on two benchmark corpora demonstrate that we can discover meaningful dialog structure, the use of GNN is crucial to dialog structure discovery, and the graph can improve dialog coherence significantly.

## 2 Related Work

### 2.1 Dialog structure learning for task-oriented dialogs

There are previous work on discovering human-readable dialog structure for task-oriented dialogs via hidden Markov models (Chotimongkol, 2008; Ritter et al., 2010; Zhai and Williams, 2014) or variational auto-encoder (Shi et al., 2019). However, the number of their dialog states is limited to only dozens or hundreds, which cannot cover fine-grained semantics in chitchat. Moreover, our method can discover a hierarchical dialog structure, which is different from the non-hierarchical dialog structures in most previous work.

### 2.2 Knowledge aware conversation generation

There are growing interests in leveraging knowledge bases for generation of more informative responses (Moghe et al., 2018; Dinan et al., 2019; Liu et al., 2019; Xu et al., 2020c,a). In this work, we employ a dialog-modeling oriented graph built from dialog corpora, instead of an external knowledge base, in order to facilitate multi-turn dialog modeling.

### 2.3 Latent variable models for chitchat

Recently, latent variables are utilized to improve diversity (Serban et al., 2017; Zhao et al., 2017; Gu et al., 2019; Gao et al., 2019; Ghandeharioun et al., 2019), control responding styles (Zhao et al., 2018; Li et al., 2020) and incorporate knowledge (Kim et al., 2020) in dialogs. Our work differs from

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³Co-occurrence means that two utterance-level vertices are mapped to two adjacent utterances in a session.
Algorithm 1 Phrase extraction

Input: An utterance \( U \)
Output: A set of phrases \( E \) extracted from \( U \)

1: Obtain a dependency parse tree \( T \) for \( U \);
2: Get all the head words \( \text{HED} \) that are connected to \( \text{ROOT} \) node, and all the leaf nodes in \( T \) (denoted as \( L \));
3: for each leaf node in \( L \) do
4: Extract a phrase consisting of words along the tree from \( \text{HED} \) to current leaf node, denoted as \( e_i \);
5: end for
6: return \( E \)

Figure 3: Overview of our algorithm “DVAE-GNN” for discovering a dialog structure graph from dialog dataset. FFN denotes feed-forward neural networks and Emb refers to embedding layers.

3 Our Approach

3.1 Problem Definition

Given a corpus \( D \) that contains \( |D| \) dialog sessions \( \{X_1, X_2, ..., X_{|D|}\} \), where each dialog session \( X \) consists of a sequence of \( c \) utterances, and \( X = [x_1, ..., x_c] \). The objective is to discover a two-layer dialog structure graph \( G = \{\mathcal{V}, \mathcal{E}\} \) from all dialog sessions in \( D \), where \( \mathcal{V} \) is the vertex set and \( \mathcal{E} \) is the edge set. Specifically, \( \mathcal{V} \) consists of two types, \( v^s_m \) (1 \( \leq \) \( m \) \( \leq \) \( M \)) for session-level vertices (topics) and \( v^n_n \) (1 \( \leq \) \( n \) \( \leq \) \( N \)) for utterance-level vertices. \( \mathcal{E} \) contains three types: edges between two session-level vertices (denoted as Sess-Sess edges), edges between two utterance-level vertices (denoted as Utter-Utter edges), and edges between an utterance-level vertex and its parent session-level vertices (denoted as Sess-Utter edges).

Figure 3 shows the proposed DVAE-GNN framework. It contains two procedures, vertex recognition and utterance reconstruction (as the role of recognition module in VAE (Kingma and Welling, 2014)), and utterance reconstruction that regenerates all utterances in sessions (as the role of decoding module in VAE).

3.2 Graph Initialization

Vertex Initialization. Theoretically, we can cold start the representation learning of vertices in dialog structure graph. In practice, to accelerate the learning procedure, we warm start each utterance-level vertex representation with the combination of two parts: one discrete latent variable and one distinct phrase. The associated phrase with each utterance-level vertex provides prior semantic knowledge for utterance-level vertex representation, which is beneficial for reducing the learning difficulty. Specifically, we first extract distinct phrases from all dialog utterances with Algorithm 1. Then we choose the top-\( N \) most frequent extracted phrases (the same number as utterance-level vertices), and then randomly match utterance-level vertices and the phrases in pairs during initialization. Notice that the association relations are not changed afterwards.

Formally, we use \( \Lambda_s \) and \( \Lambda_e \) to represent the hidden representation matrix of discrete session-level and utterance-level vertices respectively. The calculation can be shown as follows:

\[
\begin{align*}
\Lambda_s[m] &= W^s v^s_m \quad (1) \\
\Lambda_e[n] &= e(p h_n) ; W^n v^n_n \quad (2)
\end{align*}
\]

where \( \Lambda_s[m] \) denotes the representation vector of \( m \)-th session-level vertex, \( \Lambda_e[n] \) denotes the representation vector of \( n \)-th utterance-level vertex, \( v^s_m \) and \( v^n_n \) are one-hot vectors of discrete vertices, \( e(p h_n) \) denotes the representation vector of the
associated phrase $p_{h_n}$ with $v_{h_n}^u$, $W^u$ and $W^*$ are parameters, and "\|" denotes concatenation operation. Specifically, for phrase representation, we first feed word sequence in the phrase to an RNN encoder and obtain their hidden vectors. Then we compute the average pooling value of these hidden vectors as $e(p_{h_n})$.

**Edge Initialization** We build an initial Utter-Utter edge between two utterance-level vertices when their associated phrases can be extracted sequentially from two adjacent utterances in the same dialog session.

### 3.3 Vertex Recognition

#### Utterance-level Vertex Recognition.
For each utterance $x_i$ in a dialog session, we map it to an utterance-level vertex. Specifically, we first encode the utterance $x_i$ with an RNN encoder to obtain its representation vector $e(x_i)$. Then, we calculate the posterior distribution of the mapped utterance-level vertex, $z_i$, by a feed-forward neural network (FFN):

$$ z_i \sim q(z|x_i) = \text{softmax}(\mathbf{A}_s e(x_i)). \quad (3) $$

Finally, we obtain the mapped utterance-level vertex, $z_i$, by sampling from the posterior distribution with Gumbel-Softmax (Jang et al., 2017). Here, we can obtain an utterance-level vertex sequence after mapping each utterance in one dialog session, where the sequence is utilized for session-level vertex recognition.

#### Session-level Vertex Recognition.
We assume that each session-level vertex corresponds to a group of similar utterance-level vertex sequences that are mapped by different dialog sessions. And these similar sequences might have overlapped utterance-level vertices. To leverage this locally overlapping vertex information for encouraging mapping similar utterance-level vertex sequences to similar session-level vertices, we employ graph neural network to model complex relations among vertices for session-level vertex recognition. Specifically, we utilize a three-layer graph convolution network (GCN) over Utter-Utter edges to calculate structure-aware utterance-level semantics. The calculation is defined by:

$$ h_{v_n}^j = \sigma^j(\sum_{v_{n'}^u \in \mathcal{N}(v_n^u)} h_{v_{n'}^u}^{j-1}), \quad (4) $$

where $h_{v_n}^j$ denotes the $j$-th layer structure-aware representation for the $n$-th utterance-level vertex $v_n^u$. $\sigma^j$ is the sigmoid activation function for the $j$-th layer, and $\mathcal{N}(v_n^u)$ is the set of utterance-level neighbors of $v_n^u$ in the graph. Here, we can obtain a structure-aware semantic sequence $[h_{v_1}^3, h_{v_2}^3, ..., h_{v_n}^3]$, where $h_{v_n}^3$ represents the final structure-aware representation of $i$-th mapped utterance-level vertex, $v_n^u$.

Then, we feed the structure-aware semantic sequence to an RNN encoder, denoted as the vertex-sequence encoder, to obtain the structure-aware session representation $e(z_1, ..., c)$. We calculate the posterior distribution of the mapped session-level vertex, $g$, as follows:

$$ g \sim q(g|z_1, ..., c) = \text{softmax}(\mathbf{A}_s e(z_1, ..., c)). \quad (5) $$

Then, we obtain the mapped session-level vertex, $g$, by sampling from the session-level posterior distribution with Gumbel-Softmax.

### 3.4 Utterance Reconstruction

We reconstruct all utterances in the dialog session by feeding these mapped vertices into an RNN decoder (denoted as the reconstruction decoder). Specifically, to regenerate utterance $x_i$, we concatenate the representation vector of mapped utterance-level vertex $\mathbf{A}_s[z_i]$ and the representation vector of the mapped session-level vertex $\mathbf{A}_s[g]$, as the initial hidden state of the reconstruction decoder.

Finally, we optimize the DVAE-GNN model by maximizing the variational lower-bound (ELBO) (Kingma and Welling, 2014). Please refer to Appendix D for more details.

### 3.5 Graph Construction

After training DVAE-GNN, we construct the dialog structure graph with well-trained DVAE-GNN by three steps, as shown in Figure 1. Specifically, we first map all dialog sessions in corpus to vertices by Equation 3 and 5.

Then, we collect co-occurrence statistics of these mapped vertices. Specifically, we count the total mapped times for each session-level vertex, denoted as $\#(v_i^s)$, and those for each utterance-level vertex, denoted as $\#(v_j^u)$. Furthermore, we collect the co-occurrence frequency of a session-level vertex and an utterance-level vertex that are mapped by a dialog session and an utterance in it respectively, denoted as $\#(v_i^s, v_j^u)$. Moreover, we collect the co-occurrence frequency of two utterance-level vertices that are sequentially mapped by two adjacent utterances in a dialog session, denoted as $\#(v_j^u, v_k^u)$. 

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Finally, we build edges between vertices based on these co-occurrence statistics. We first build a directed Utter-Utter edge from \( v^u_j \) to \( v^u_k \) if the bi-gram transition probability \( \#(v^u_j, v^u_k) / \#(v^u_j) \) is above a threshold \( \alpha^{uu} \). Then, we build a bidirectional Sess-Utter edge between \( v^u_k \) and \( v^u_k \) if the probability \( \#(v^u_k, v^u_k) / \#(v^u_k) \) is above a threshold \( \alpha^{su} \). Moreover, we build a directed Sess-Sess edge from \( v^u_k \) to \( v^u_k \), if \( \#(v^u_k, v^u_k) / \#(v^u_k) \) is above a threshold \( \alpha^{ss} \), where the first item \( \#(v^u_k, v^u_k) \) is the number of utterance-level vertices that are connected to both session-level vertices. Here, Sess-Sess edges are dependent on Sess-Utter edges.

### 3.6 Graph Grounded Dialog Generation

To prove the effectiveness of the discovered structure for coherent dialog generation, we utilize a graph grounded conversation system (GCS) following (Xu et al., 2020a). Different from single-layer policy in Xu et al. (Xu et al., 2020a), we present a hierarchical policy for two-level vertex selection. The GCS contains three modules: (1) a dialog context understanding module that maps given dialog context (the previous two utterances) to an utterance-level vertex (called as hit utterance-level vertex) in the graph with well-trained DVAE-GNN, (2) a hierarchical policy that learns to walk over one-hop graph edges (for dialog coherence) to select an utterance-level vertex to serve as response content, and (3) a response generator that generates an appropriate response based on the selected utterance-level vertex. Specifically, a session-level sub-policy first selects a session-level vertex as current dialog topic. Then, an utterance-level sub-policy selects an utterance-level vertex from current dialog topic’s child utterance-level vertices.

**Session-level sub-policy** Let \( A^g_{si} \) denote the set of session-level candidate actions at time step \( l \). It consists of all parent session-level vertices of the hit utterance-level vertex. Given current RL state \( s_i \) at the time step \( l \), the session-level sub-policy \( \mu^g \) selects an appropriate session-level vertex from \( A^g_{si} \) as the current dialog topic. Specifically, \( \mu^g \) is formalized as follows:

\[
\mu^g(s_i, v^g_j) = \frac{\exp(e_{s_i}^T A^g_{s_i} [v^g_j])}{\sum_{k=1}^{N^g_{si}} \exp(e_{s_i}^T A^g_{s_i} [v^g_k])},
\]

where \( e_{s_i} \) is the aforementioned RL state representation, \( v^g_j \) the \( j \)-th session-level vertex in \( A^g_{si} \), and \( N^g_{si} \) the number of session-level vertices in \( A^g_{si} \).

**Utterance-level sub-policy** Let \( A^u_{si} \) denote the set of utterance-level candidate actions at time step \( l \). It consists of utterance-level vertices that are connected to the vertex of current dialog topic. Given current state \( s_i \) at the time step \( l \), the utterance-level sub-policy \( \mu^u \) selects an optimal utterance-level vertex from \( A^u_{si} \). Specifically, \( \mu^u \) is defined as follows:

\[
\mu^u(s_i, v^u_j) = \frac{\exp(e_{s_i}^T A^u_{s_i} [v^u_j])}{\sum_{k=1}^{N^u_{si}} \exp(e_{s_i}^T A^u_{s_i} [v^u_k])},
\]

Here, \( e_{s_i} \) is the aforementioned RL state representation, \( v^u_j \) the \( j \)-th utterance-level vertex in \( A^u_{si} \), and \( N^u_{si} \) the number of utterance-level candidate vertices in \( A^u_{si} \). With the distribution calculated by the above equation, we utilize Gumbel-Softmax to sample an utterance-level vertex from \( A^u_{si} \), to provide response content for response generator, which is a Seq2Seq model with attention mechanism.

To train RL, we use a set of rewards including utterance relevance, utter-topic closeness, and repetition penalty. For the session-level sub-policy, its reward \( r^g \) is the average rewards from the utterance-level sub-policy during current dialog topic. The reward for the utterance-level sub-policy, \( r^u \), is a weighted sum of the below-mentioned factors. The default values of weights are set as [60, 0.5, -0.5].

i) **Utterance relevance** We choose the classical multi-turn response selection model, DAM in (Zhou et al., 2018), to calculate utterance relevance. We expect the generated response is coherent to dialog context.

ii) **Utter-topic closeness** The selected utterance-level vertex \( v^u_j \) should be closely related to current topic \( v^u_k \). And we use the \( \#(v^u_k, v^u_j) / \#(v^u_k) \) in Section 3.5 as the utter-topic closeness score.

iii) **Repetition penalty** This factor is 1 when the selected utterance-level vertex shares more than 60% words with one of contextual utterance, otherwise 0. We expect that the selected utterance-level vertices are not only coherent, but also diverse.

Further implementation details can be found in the Appendix C.

### 4 Experiments for Dialog Structure Graph Discovery

#### 4.1 Datasets and Baselines

We evaluate the quality of dialog structure graph discovered by our method and baselines on two

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1We optimize these weights by grid search.
Datasets | Methods | Automatic Evaluation | Human Evaluation |
|-------|--------|----------------------|-----------------|
|       |        | NLL   | BLEU-1/2. | S-U Appr. | U-U Appr. | Sess-V.-Qual. |
|       |        |       |           | (Multi-turn coherence) | (Single-turn coherence) | (Multi-turn coherence) |
| Weibo | DVRNN  | 29.187 | 0.427/0.322 | - | 0.16 | - |
|       | Phrase Graph | - | - | - | 0.63 | - |
|       | DVAE-GNN | 20.969 | 0.588/0.455 | 0.85 | 0.79 | 1.44 |
|       | DVAE-GNN w/o GNN | 23.364 | 0.560/0.429 | 0.53 | 0.78 | 1.06 |
|       | DVAE-GNN w/o phrase | 24.282 | 0.468/0.355 | 0.43 | 0.27 | 0.95 |
| Douban| DVRNN  | 72.744 | 0.124/0.093 | - | 0.14 | - |
|       | Phrase Graph | - | - | - | 0.34 | - |
|       | DVAE-GNN | 35.975 | 0.525/0.412 | 0.60 | 0.70 | 0.93 |
|       | DVAE-GNN w/o GNN | 37.415 | 0.504/0.394 | 0.38 | 0.54 | 0.48 |
|       | DVAE-GNN w/o phrase | 49.606 | 0.254/0.206 | 0.28 | 0.19 | 0.27 |

Table 1: Evaluation results for dialog structure graphs extracted from Weibo corpus or Douban corpus. As DVRNN learns only utterance-level states, its results in terms of S-U Appr. and Sess.V.-Qual. are not available.

benchmark datasets: (1) **Weibo** (Li and Yan, 2018): this is a Chinese multi-turn tweet-style corpora. After data cleaning, we obtain 3.1 million sessions for training, 10k sessions for validation and 10k sessions for testing. (2) **Douban** (Wu et al., 2017): we use the original multi-turn dialog corpus, and obtain 2.3 million sessions for training, 10k sessions for validation and 10k sessions for testing. For the Weibo or Douban corpus, each dialog session has 4 sentences on average, and each sentence contains about 7 or 14 words respectively. The discovered dialog structure graph on Weibo corpus contains 1,641,238 utterance-level vertices, 6000 session-level vertices and 11,561,007 edges. And the discovered dialog structure graph on Douban corpus contains 1,768,720 utterance-level vertices, 5500 session-level vertices and 6,117,159 edges. The number of utterance-level vertices is equal to the number of extracted phrase number in corpus and session-level vertices is determined by grid search based on the NLL metric in Section 4.2.

In this work, we select DVRNN (Shi et al., 2019) as a baseline, since there is few previous study on unsupervised open-domain dialog structure discovery. DVRNN is the SOTA unsupervised method in discovering dialog structure in task-oriented dialogs, which outperforms other hidden Markov based methods by a large margin (Shi et al., 2019). We rerun the original source codes. Notice that, to suite the setting of open-domain dialog and also consider the limit of our 16G GPU memory (we set batch size as 32 to ensure training efficiency), we set the number of dialog states as 50 (originally it is 10).7 We also evaluate the quality of the initialized graph (denoted as Phrase Graph) that consists of only phrases (as vertices) and initial edges (between phrases) in Section 3.2. For more details, please refer to Appendix A.1.

4.2 Evaluation Metrics

We evaluate discovered dialog structure graph with both automatic evaluation and human evaluation. For automatic evaluation, we use two metrics to evaluate the performance of reconstruction: (1) **NLL** is the negative log likelihood of dialog utterances; (2) **BLEU-1/2** measures how much that reconstructed sentences contains 1/2-gram overlaps with input sentences (Papineni et al., 2002). The two metrics indicate how well the learned dialog structure graph can capture important semantic information in dialog dataset.

Further, we manually evaluate the quality of edges and vertices in the graph. For edges, (1) **S-U Appr.** for multi-turn dialog coherence. It measures the appropriateness of Sess-Utter edges, where these edges provide crucial prior information to ensure multi-turn dialog coherence (see results in Section 5.4). “1” if an utterance-level vertex is relevant to its session-level vertex (topic), otherwise “0”. (2) **U-U Appr.** for single-turn dialog coherence: It measures the quality of Utter-Utter edges between two utterance-level vertices, where these edges provide crucial prior information to...
ensure single-turn dialog coherence. It is “1” if an Utter-Utter edge is suitable for responding, otherwise “0”. Notice that we don’t evaluate the quality of Sess-Sess edges because Sess-Sess edges are dependent on the statistics of Sess-Utter edges.

Meanwhile, for vertices, we evaluate Session-level Vertex Quality (Sess.V.-Qual.). Ideally, a session-level vertex (topic) should be mapped by dialog sessions that share high similarity. In other words, we can measure the quality of a session-level vertex by evaluating the similarity of semantics between two sessions that are mapped to it. It is “2” if the two sessions mapped to the same session-level vertex are about the same or highly similar topic, “0” if the two sessions contains different topic, otherwise “1”. Specifically, during evaluation, we provide typical words of each topic by calculating TF-IDF on utterances that are mapped to it. High “Sess.V.-Qual.” is beneficial to conduct topic management for coherent multi-turn dialogs.

For human evaluation, we sample 300 cases and invite three annotators from a crowd-sourcing platform to evaluate each case. Notice that all system identifiers are masked during human evaluation.

### 4.3 Experiment Results

As shown in Table 1, DVAE-GNN significantly outperforms DVRNN, in terms of all the metrics (sign test, p-value < 0.01) on the two datasets. It demonstrates that DVAE-GNN can better discover meaningful dialog structure graph. Specifically, DVAE-GNN obtains the best results in terms of NLL and BLEU-1/2, which shows that DVAE-GNN can better capture important semantic information in comparison with DVRNN. Meanwhile, DVAE-GNN also surpasses all baselines in terms of “U-U Appr.” and “S-U Appr.”. It indicates that our discovered dialog structure graph has higher-quality edges and can better facilitate coherent dialog generation.

Furthermore, we conduct ablation study. Specifically, to evaluate the contribution of GNN, we remove GNN from DVAE-GNN, denoted as DVAE-GNN w/o GNN. We see that its performance drop sharply in terms of “S-U Appr.” and “Sess.V.-Qual.”. It demonstrates that GNN can better incorporate the structure information (complex relations among vertices) into session-level vertex representation learning. Moreover, to evaluate the contribution of phrases to utterance-level vertex representation, we remove phrases, denoted as DVAE-GNN w/o phrase. We see that its scores in terms of all the metrics drops sharply, especially the three human evaluation metrics. The reason is that it’s difficult to learn high-quality utterance-level vertex representation from a large amount of fine-grained semantic content in open-domain dialogs without any prior information. The Kappa value is above 0.4, showing moderate agreement among annotators.

Two sample parts of the discovered dialog structure graph can be found in Appendix B.

### 5 Experiments for Graph Grounded Dialog Generation

To confirm the benefits of discovered dialog structure graph for coherent conversation generation, we conduct experiments on the graph discovered from Weibo corpus. All the systems (including baselines) are trained on Weibo corpus.

#### 5.1 Models

We carefully select the following six baselines.

- **MMPMS** It is the multi-mapping based neural open-domain conversational model with posterior mapping selection mechanism (Chen et al., 2019), which is a SOTA model on the Weibo Corpus.
- **MemGM** It is the memory-augmented open-domain dialog model (Tian et al., 2019), which learns to cluster U-R pairs for response generation.
- **HRED** It is the hierarchical recurrent encoder-decoder model (Serban et al., 2016).
- **CVAE** It is the Conditional Variational Auto-Encoder based neural open-domain conversational model (Zhao et al., 2017).
- **VHCR-EI** This variational hierarchical RNN model can learn hierarchical latent variables from open-domain dialogs (Ghandeharioun et al., 2019). It is a SOTA dialog model with hierarchical VAE.
- **DVRNN-RL** It discovers dialog structure graph for task-oriented dialog modeling (Shi et al., 2019).

**GCS** It is our proposed dialog structure graph grounded dialog system with hierarchical RL.

**GCS w/ UtterG** It is a simplified version of GCS that just uses the utterance-level graph and utterance-level sub-policy.

**GCS w/ Phrase Graph** It is a simplified version of GCS that just uses the phrase graph and utterance-level sub-policy.
Table 2: Evaluation results for baselines and our system trained on Weibo corpus. ∗ or # denote human or automatic evaluation metrics.

We use the same user simulator for RL training of DVRNN-RL, GCS and GCS w/ UtterG. Here, we use the original MMPMS as user simulator because it achieves the best result on the Weibo Corpus. The user simulator is pre-trained on dialog corpus and not updated during policy training. We use the original source codes for all the baselines and the simulator. Further details about baselines and GCS can be found in Appendix A.2.

We conduct model-human dialogs for evaluation. Given a model, we first randomly select an utterance (the first utterance in a session) from test set for the model side to start the conversations with a human turker. Then the human is asked to converse with the selected model till 8 turns are reached. Finally, we obtain 50 model-human dialogs for multi-turn evaluation. Then we randomly sample 200 U-R pairs from the above dialogs for single-turn evaluation.

### 5.2 Evaluation Metrics

Since the proposed system does not aim at predicting the highest-probability response at each turn, but rather the long-term success of a dialog (e.g., coherence), we do not employ BLEU (Papineni et al., 2002) or perplexity for evaluation. We use three multi-turn evaluation metrics and three single-turn metrics. For human evaluation, we invite three annotators to conduct evaluation on each case, and we ask them to provide 1/0 (Yes or No) scores for most of the metrics. Moreover, for multi-turn coherence, we first ask the annotators to manually segment a dialog by topics and then conduct evaluation on each session. A session refers to a dialog fragment about one topic. Notice that system identifiers are masked during human evaluation.

#### Multi-turn Metrics

We use the following metrics: (1) **Multi-turn Coherence (Multi.T.-Coh.)** It measures the coherence within a session. Common incoherence errors in a session include amphi
or errors across utterances and information inconsistency. “0” means that there are more than two incoherence errors in a session. “1” means that there are only one error. “2” means that there are no errors. Finally, we compute the average score of all the sessions. (2) **Dialog engagement (Enga.)** This metric measures how interesting a dialogs is. It is “1” if a dialog is interesting and the human is willing to continue the conversation, otherwise “0”. (3) **Length of high-quality dialog (Length)** A high-quality dialog ends if the model tends to produce dull responses or two consecutive utterances are highly overlapping (Li et al., 2016b).

#### Single-turn Metrics

We use the following metrics: (1) **Single-turn Coherence (Single.T.-Coh.)** “0” if a response is inappropriate as an reply, otherwise “1”; (2) **Informativeness (Info.)** “0” if a response is a “safe” response, e.g. “I don’t know”, or it is highly overlapped with context, otherwise “1”; (3) **Distinct (Dist.-i)** It is an automatic metric for response diversity (Li et al., 2016a).

### 5.3 Experiment Results

As shown in Table 2, GCS significantly outperforms all the baselines in terms of all the metrics except “Length-of-dialog” (sign test, p-value < 0.01). It indicates that GCS can generate more coherent, informative and engaging dialogs. Specifically, our system’s two sub-policies strategy on the dialog structure graph enables more coherent dialog flow control than hierarchical latent variable based VHCR-EI model that performs the best among
国庆节快到了，我快放假了。
User 我放假了，我们可以出去玩了，放风筝。
Bot 好的呀，哈哈哈，那就带着你大餐[Great! Looking forward to your big meal.]
User 哈哈，我想去南京旅游，一起去吧[Well, I want to travel to Nanjing, let’s go together.]
Bot 不要了！[I feel like you’re abandoning me.]
User 要你了，咱们一起去[No, you can come with us.]

Start 我会化妆了 给你化妆了，[National Day is coming, I’m going to have a holiday.]
Bot 你太好了，你化妆后 我会来接你[You’re so nice, I’ll come to pick you up.]
User 那你好棒棒[You are so generous. How could such a good thing happen.

Figure 4: A sample dialog between our dialog system GCS and a human, where “Bot” is our system and “User” is the human. This dialog contains three dialog topics. We translate the original Chinese texts into English language.

Ablation Study. In order to evaluate the contribution of session-level vertices, we run GCS with an utterance-level dialog structure graph, denoted as “GCS w/ UtterG”. Results in Table 2 show that its performance in terms of “Multi.T.-Coh.” and “Enga.” drops sharply. It demonstrates the contribution of our hierarchical dialog structure graph for enhancing dialog coherence and dialog engagement. The possible reason for the inferior performance of “GCS w/ UtterG” is that the removal of session-level vertices harms the capability of selecting coherent utterance-level vertex sequence.

6 Conclusion

In this paper, we conduct unsupervised discovery of discrete dialog structure from chitchat corpora. Further, we try to formalize the structure as a two-layer directed graph. To discover the dialog structure, we present an unsupervised model, DVAE-GNN, which integrates GNN into DVAE to model complex relations among dialog states for more effective dialog structure discovery. Experimental results demonstrate that DVAE-GNN can discover meaningful dialog structure, and the use of dialog structure as background knowledge can significantly improve multi-turn dialog coherence.

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A Implementation Details

A.1 Implementation Details about DVAE-GNN

For all models, we share the same vocabulary (maximum size is 50000) and initialized word embedding (dimension is 200) with the pre-trained Tencent AI Lab Embedding.9 Meanwhile, we randomly initialized the embedding space of session-level vertices and latent vectors for utterance-level vertices (dimensions are 200). The hidden sizes of all RNN encoders and RNN decoders are set as 512. The three threshold variables about co-occurrence statistics $\alpha^{uu}$, $\alpha^{su}$ and $\alpha^{ss}$ are all set as 0.05.

We use the PaddlePaddle framework for the development of our systems.10 Notice that it is costly to calculate Equation 3 in Section 3.3 since the total number of utterance-level vertices, $N$, is very large (more than one million). In practice, for each utterance, we first retrieve the top-50 most related utterance-level vertices according to Okapi BM25 (Robertson and Zaragoza, 2009) similarity between the utterance and associated phrases of all candidate vertices. And then calculate Equation 3 only with these retrieved vertices. Thus, only a part of vectors in $\Lambda_x$ will be dynamically updated for each training sample when training DVAE-GNN.

A.2 Experiment settings about GCS

Source codes about baselines

- HRED: github.com/julianser/hed-dlg-truncated
- MMPMS: github.com/PaddlePaddle/Research/tree/master/NLP/IJCAI2019-MMPMS
- CVAE: github.com/snakeztc/NeuralDialog-CVAE
- VHCR-EI: github.com/natashamjaques/neural_chat
- MemGM: github.com/tianzhiliang/MemoryAugDialog
- DVRNN: github.com/wyshi/Unsupervised-Structure-Learning

Hyper-parameter Setting for Training In our experiments, all the models share the same vocabulary (maximum size is 50000 for both Weibo corpus and Douban corpus), initialized word embedding (dimension is 200) with the Tencent AI Lab Embedding. Moreover, bidirectional one-layer GRU-RNN (hidden size is 512) is utilized for all the RNN encoders and RNN decoders. In addition, dropout rate is 0.3, batch size is 32 and optimizer is Adam(lr=2e-3) for all models. During RL training, the discounting weight for rewards is set as 0.95. The MMPMS model for the user simulator employs 10 responding mechanisms. We utilize dependency parse for phrase extraction.11 We pre-train the response generator in the Weibo Corpus.

Rewards and Training Procedure for the Graph grounded Conversational System. We use the PaddlePaddle framework for the development of our systems.12 We hot-start the response generator by pre-training it before the training of policy module. Meanwhile, to make the RL based training process more stable, we employ the A2C method (Sutton and Barto, 2018) for model optimization rather than the original policy gradient as done in previous work (Li et al., 2016b). Moreover, during RL training, the parameters of the policy module are updated, and the parameters of response generator and the representation of semantic vertices stay intact.

B Case Study of Dialog Structure Graph Discovery

Figure 5 shows a part of the unified dialog structure graph that is discovered from the Weibo corpus. Each yellow-colored circle in this figure represents a session-level vertex with expert interpreted meanings based on the information of top words (from phrases of utterance-level vertices belonging to this session-level vertex) ranked by TF/IDF. Each green-colored rectangle represents an utterance-level vertex. The directed-arrows between utterance-level vertices represent dialog transitions between states, and the utterance-level vertices within blue dotted-lines are about the same session-level vertex (topic).

We observe reasonable dialog structures in Figure 5. It captures the major interaction logic in dialogs about the topic “go traveling”, traveling is really good $\rightarrow$ you decide where to travel $\rightarrow$ let’s
出去旅游
Go traveling
找个男朋友
Want a boyfriend
好久没出去旅游
Haven't been traveling for a long time
出去旅游真好
Travel is really good
应该带上一个西安人
Should travel with a Xi'an people
想回到以前的西安
Want to go back to historical Xi'an
等我一起去看兵马俑
Wait for me to see the Terracotta Warriors

大声告诉我你的目标
Tell me your goal loudly
找个会照相的男朋友
Find a boyfriend who can take good pictures
会让人羡慕
Been slightly enviable
拍出好看的照片
Take beautiful pictures
真心觉得好看
It really looks good
单身的女孩要先坚强
Single girls need to be strong first

你好烦
You are so boring
这样找不到对象
Will never have a boyfriend
找男朋友干嘛
What's a boyfriend for
可以陪我过节日
Can accompany me to celebrate the festival

Figure 5: A part of the unified dialog structure graph that is extracted from Weibo corpus. Here, we interpret session-level semantics based on their child utterance-level vertices. We translate the original Chinese texts into English language.

Figure 6: A part of the unified dialog structure graph that is extracted from Weibo corpus. Here, we interpret session-level semantics based on their child utterance-level vertices. We translate the original Chinese texts into English language.
go to Huangshan → comments about Huangshan. Furthermore, it also captures the major logic in dialogs about the topic “want a boyfriend”, need a boyfriend → why? → he can accompany me to celebrate the festival. Moreover, it captures a dialog topic transition between the topic “go traveling” and another topic “want a boyfriend”.

Figure 6 shows another part of the unified dialog structure graph that discovered from the Weibo corpus.

C GCS with RL

In the following, we will elaborate the details of GCS.

C.1 Dialog Context Understanding

Given a dialog context (the last two utterances), we first map it to the graph by recognizing the most related utterance-level vertex with the well-trained DVAE-GNN. Here, the recognized utterance-level vertex is denoted as the hit utterance-level vertex.

For policy learning, we build current RL state $s_t$ at time step $t$ by collecting dialog context (the last two utterances), previously selected session-level vertex sequence, and previously selected utterance-level vertex sequence. Here, we first utilize three independent RNN encoders to encode them respectively, and then concatenate these three obtained representation vectors, to obtain the representation of the RL state, $e_s$.

C.2 Response Generator

The response generator is a pre-trained Seq2Seq model with attention mechanism, whose parameters are not updated during RL training. Specifically, we take the last user utterance, and the associated phrase of the selected utterance-level vertex as input of the generator.

D Training Objective for DVAE-GNN

The proposed DVAE-GNN model consists of two procedures. In the recognition procedure, for a dialog session $X$ that consists of a sequence of $c$ utterances, $X = \{x_1, ..., x_c\}$, in recognition procedure, we first recognize an utterance-level vertex $z_i$ for each utterance $x_i$, and then recognize a session-level vertex $g$ based on all recognized utterance-level vertices, $[z_1, ..., z_c]$. In reconstruction procedure, we regenerate all the utterances in $X$ with the predicted vertices $Z = \{z_1, ..., z_c, g\}$. Here, we optimize the proposed DVAE-GNN model by maximizing the variational lower-bound:

$$E_q(Z|X)[log p(X|Z)] − KL(q(Z|X)||p(Z)),$$

where $p(Z)$ is the prior uniform distribution of $Z$.

Specifically, we approximate the first item in the above equation by sampling $Z$ from $q(Z|X)$ and calculate the the negative log-likelihood reconstruction loss. For the second item, we calculate it by:

$$\sum_j^c KL[q(z_j|x_j)||p(z_j)] + KL[q(g|z_1,...,c)||p(g)],$$

where we can calculate each sub-item straightly since $z_1,...,c$ and $g$ follow discrete distribution. Below, we provide the derivation of the second item.

$$KL[q(Z|X)||p(Z)]$$

$$= \sum_i^x \log q(Z|X) − \log p(Z|X)$$

$$= \sum_i^x (\sum_j^z \log q(z_j|x_j) − \log p(z_j)) + \sum_j^z \log p(z_j)$$

$$= \sum_j^c KL[q(z_j|x_j)||p(z_j)] + KL[q(g|z_1,...,c)||p(g)]$$