Probing light mediators and \((g - 2)\mu\) through detection of coherent elastic neutrino nucleus scattering at COHERENT

M. Atzori Corona,\(^a\) M. Cadeddu,\(^b\) N. Cargioli,\(^a\) F. Dordei,\(^b\) C. Giunti,\(^c\) Y.F. Li,\(^d,e\) E. Picciau,\(^a\) C.A. Ternes\(^c\) and Y.Y. Zhang\(^d,e,1\)

\(^a\)Dipartimento di Fisica, Università degli Studi di Cagliari, Complesso Universitario di Monserrato — S.P. per Sestu Km 0.700, 09042 Monserrato (Cagliari), Italy

\(^b\)Istituto Nazionale di Fisica Nucleare (INFN), Sezione di Cagliari, Complesso Universitario di Monserrato — S.P. per Sestu Km 0.700, 09042 Monserrato (Cagliari), Italy

\(^c\)Istituto Nazionale di Fisica Nucleare (INFN), Sezione di Torino, Via P. Giuria 1, I-10125 Torino, Italy

\(^d\)Institute of High Energy Physics, Chinese Academy of Sciences, Beijing 100049, China

\(^e\)School of Physical Sciences, University of Chinese Academy of Sciences, Beijing 100049, China

E-mail: mattia.atzori.corona@ca.infn.it, matteo.cadeddu@ca.infn.it, nicola.cargioli@ca.infn.it, francesca.dordei@cern.ch, carlo.giunti@to.infn.it, liyufeng@ihep.ac.cn, emmanuele.picciau@ca.infn.it, ternes@to.infn.it, zhangyiyu@ihep.ac.cn

ABSTRACT: We present the constraints on the parameters of several light boson mediator models obtained from the analysis of the current data of the COHERENT CEνNS experiment. We consider a variety of vector boson mediator models: the so-called universal, the \(B - L\) and other anomaly-free \(U(1)'\) gauge models with direct couplings of the new vector boson with neutrinos and quarks, and the anomaly-free \(L_\mu - L_\tau\), \(L_\mu - L_\tau\), and \(L_\mu - L_\tau\) gauge models where the coupling of the new vector boson with the quarks is generated by kinetic mixing with the photon at the one-loop level. We consider also a model with a new light scalar boson mediator that is assumed, for simplicity, to have universal coupling with quarks and leptons. Since the COHERENT CEνNS data are well-fitted with the cross section predicted by the Standard Model, the analysis of the data yields constraints for the mass and coupling of the new boson mediator that depend on the charges of quarks and neutrinos in each model under consideration. We compare these constraints with the limits obtained in other experiments and with the values that can explain the muon \(g - 2\) anomaly in the models where the muon couples to the new boson mediator.

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\(^1\)Corresponding author.
1 Introduction

The discovery of coherent elastic neutrino-nucleus scattering (CEνNS) in cesium-iodide (CsI) by the COHERENT Collaboration [1, 2] sparked a flood of research into a variety of physical processes, with substantial implications for particle physics, astrophysics, nuclear physics, and beyond [3–10, 10–20]. After the discovery in 2017 of CEνNS with the CsI detector, the COHERENT Collaboration accomplished in 2020 the first observation of CEνNS in argon (Ar) [21, 22] and updated in 2021 the results obtained with the CsI detector [23]. By combining the greater CEνNS statistics with a refined quenching factor estimation for the CsI measurement and by virtue of the complementary role of two different target nuclei, more stringent tests of nuclear physics, neutrino properties, electroweak interactions, and new physics beyond the Standard Model (SM) have been performed [24–28].
The CEνNS process happens when the momentum transfer between the incoming neutrino and the target nucleus is so small that the wavelength of the boson which mediates the interaction is larger than the nuclear radius, so that the neutrino interacts with the nucleus as a whole and the cross section is proportional to the square of the number of nucleons participating to the process. The CEνNS process is a pure neutral current interaction which is mediated by the exchange of the $Z$ vector boson in the SM, but it can also receive contributions from other hypothetical neutral bosons in theories beyond the SM. Therefore, it turns out to be a powerful tool to probe new physics interactions beyond the SM [5–10].

In this paper we test new physics models with interactions mediated by a light vector or scalar boson that contribute to the CEνNS process by analyzing the recently released 2021 CsI data [23] and the 2020 Ar data [21, 22] of the COHERENT experiment. For each model, we present the constraints on the mass and coupling of the light vector or scalar boson mediator that we obtained from the separate and combined fits of the CsI and Ar COHERENT CEνNS data. Comparing with the previous publication in ref. [26], we have considered a larger variety of vector mediator models, we have included the scalar mediator model, and we have updated the analysis using the recently released 2021 CsI data [23].

We also consider the possible explanation of the 4.2σ difference between the SM prediction [29–54] of the value of the muon anomalous magnetic moment $(g - 2)_\mu$ and the combination of the values measured at the Brookhaven National Laboratory [55] and recently at the Fermi National Laboratory [56]. This so-called $(g - 2)_\mu$ anomaly is a putative signal of physics beyond the SM, which has been studied in many papers (see, e.g., refs. [57, 58]). Interestingly, several light vector mediator models are regarded as candidate solutions (see, e.g., refs. [59–67]), but also a light scalar mediator have the potential to solve the anomaly [68]. Among the models that we consider in this paper, those in which the muon interacts with the new light boson mediator can explain the $(g - 2)_\mu$ anomaly. For these models, we compare the constraints on the mass and coupling of the new light boson mediator obtained from the analysis of the COHERENT CEνNS data and those obtained by other experiments focusing on the parameter region that can solve the $(g - 2)_\mu$ anomaly. There are many studies of extensions of the SM with the addition of a $U(1)'$ gauge group with an associated neutral vector gauge boson $Z'$ (see, e.g., the review in ref. [69]). The models differ in the charges of the fermions, which determine the contributions to CEνNS of the interactions mediated by the $Z'$ vector boson. These contributions add coherently to the SM weak neutral current interactions which are mediated by the $Z$ vector boson. The effects are quantified by additional terms in the weak charge of the nucleus. Note that the effects on the CEνNS process of the interactions mediated by a light boson are different from those induced by the so-called non-standard interactions (NSI), that arise in an effective four-fermion theory in which the heavy mediator has been integrated out. In the case of NSI there is a global rescaling of the CEνNS cross section that depends on the interaction parameters of the NSI, whereas a light boson mediator can alter the nuclear recoil energy spectrum through the boson propagator that depends on the momentum transfer. This effect generates distinct spectral features that can be probed with the experimental observations.

In this paper we first consider the so-called universal $Z'$ model in which all the standard fermions have the same charge [6, 12, 14, 15, 26, 70, 71]. This model is not anomaly-free per
se, but it can be extended with new non-standard particles to make it anomaly-free. Then, we consider several U(1)' models in which quarks and leptons have appropriate non-zero charges that cancel the quantum anomalies (e.g., the popular $B - L$ model [69, 72, 73], where $B$ is the baryon number and $L$ is the total lepton number). Since in these models the $Z'$ vector boson interacts directly with neutrinos and nucleons, the CEνNS process occurs at tree level and it is possible to obtain stringent constraints on the mass and coupling of the new vector boson from the COHERENT CEνNS data.

We also consider the anomaly-free $L_e - L_\mu$, $L_e - L_\tau$, and $L_\mu - L_\tau$ U(1)' models [74–77] (where $L_\alpha$ are the lepton generation numbers, for $\alpha = e, \mu, \tau$) in which the charges are exclusively leptonic. However, in these models there are contributions to the CEνNS process, which occur through the kinetic mixing of the $Z'$ boson with the photon, that is generated at one-loop level [28, 78, 79], and the interaction of the photon with the protons in the target nuclei. Therefore, we can constrain the mass and coupling of the vector boson in these models using the COHERENT CEνNS data, albeit less tightly than in the models with direct quark-$Z'$ interactions, because of the weaker one-loop interaction.

We consider also contributions to the CEνNS process of interactions mediated by a light scalar boson [7, 10, 80–82], which differ from those mediated by a light vector boson for the following two fundamental reasons. First, the helicity-flipping interactions mediated by a scalar boson contribute incoherently to the CEνNS process with respect to the helicity-conserving SM contribution, contrary to the helicity-conserving interactions mediated by a new vector boson that contribute coherently. Therefore, in the scalar case, the new contribution consists in an addition to the cross section, not to the amplitude of the process as in the vector case. Second, the scalar charges of the nucleons are not simply given by the sum of the charges of the valence quarks as in the vector case, because the scalar currents are not conserved as the vector currents. Therefore, the scalar charges of the nucleons must be calculated and the results have large theoretical uncertainties.

The paper is organized as follows. In section 2 the method of the COHERENT data analysis is described. In section 3, we present the cross section of the CEνNS process and summarize the models of light mediators and the corresponding effects on the CEνNS cross section. In section 4, the COHERENT CEνNS constraints on the allowed parameter space of the light mediator models are presented and compared with the $(g - 2)_\mu$ allowed regions and other current limits. Finally, we conclude and summarize our results in section 5.

2 COHERENT data analysis

The CEνNS event energy spectra in the COHERENT experiment depend on the neutrino flux produced by the pion decay. The total differential neutrino flux is given by the sum of the three neutrino components, where the first prompt component is coming from the pion decay ($\pi^+ \to \mu^+ + \nu_\mu$), and the second two delayed components are coming from the
subsequent muon decay \((\mu^+ \rightarrow e^+ + \nu_e + \bar{\nu}_\mu)\)

\[
\frac{dN_{\nu_e}}{dE} = \eta \delta \left( E - \frac{m^2_\pi - m^2_\mu}{2m_\pi} \right),
\]

\[
\frac{dN_{\nu_\mu}}{dE} = \eta \frac{64E^2}{m^3_\mu} \left( \frac{3}{4} - \frac{E}{m_\mu} \right),
\]

\[
\frac{dN_{\bar{\nu}_e}}{dE} = \eta \frac{192E^2}{m^3_\mu} \left( \frac{1}{2} - \frac{E}{m_\mu} \right).
\]

Here, \(E\) is the neutrino energy, \(m_\pi\) and \(m_\mu\) are the pion and muon masses, and \(\eta = rN_{\text{POT}}/4\pi L^2\) is the normalization factor, where \(r\) is the number of neutrinos per flavor produced for each proton-on-target (POT), \(N_{\text{POT}}\) is the number of POT, and \(L\) is the baseline between the source and the detector. For the COHERENT Ar detector, called CENNS-10, we use \(r = 0.09, N_{\text{POT}} = 13.7 \cdot 10^{22}\) and \(L = 27.5\) m [22]. For the COHERENT CsI detector, we use \(r = 0.0848, N_{\text{POT}} = 3.198 \cdot 10^{23}\) and \(L = 19.3\) m [23].

The theoretical CE\(\nu\)NS event number \(N^\text{CE\(\nu\)NS}_i\) in each nuclear-recoil energy-bin \(i\) is given by

\[
N^\text{CE\(\nu\)NS}_i = N(N) \int_{T_{nr}^i}^{T_{nr}^i + 1} dT_{nr} A(T_{nr}) \int_0^{T_{nr}^{\text{max}}} dT'_{nr} R(T_{nr}, T'_{nr}) \int_{E_{\text{min}}(T'_{nr})}^{E_{\text{max}}(T'_{nr})} dE \sum_{\nu = \nu_e, \nu_\mu, \bar{\nu}_e} \frac{dN_{\nu}}{dE}(E) \frac{d\sigma_{\nu-N}}{dT_{nr}}(E, T'_{nr}),
\]

where \(T_{nr}\) is the reconstructed nuclear recoil kinetic energy, \(T'_{nr}\) is the true nuclear recoil kinetic energy, \(A(T_{nr})\) is the energy-dependent detector efficiency, \(R(T_{nr}, T'_{nr})\) is the energy resolution function, \(T_{nr}^{\text{max}} = 2E_{\text{max}}^2/M, E_{\text{max}} = m_\mu/2 \approx 52.8\) MeV, \(E_{\text{min}}(T'_{nr}) = \sqrt{MT_{nr}^2/2}\), \(m_\mu\) being the muon mass, \(M\) the nuclear mass, and \(N(N)\) the number of \(N\) atoms in the detector. We obtained information on these quantities from refs. [21, 22] for the Ar data and from ref. [23] for the CsI data. The number of \(N\) atoms in each detector is given by \(N(N) = N_A M_{\text{det}}/M_N\), where \(N_A\) is the Avogadro number, \(M_{\text{det}}\) is the detector active mass \((M_{\text{det}} = 24\) kg for Ar and \(M_{\text{det}} = 14.6\) kg for CsI), and \(M_N\) is the molar mass \((M_{\text{Ar}} = 39.96\) g/mol and \(M_{\text{CsI}} = 259.8\) g/mol). The differential CE\(\nu\)NS cross section \(d\sigma_{\nu-N}/dT_{nr}\) is discussed in section 3.

Due to the quenching effect, the energy actually observed is the electron-equivalent recoil energy \(T_{ee}\), which is transformed into the nuclear recoil energy \(T_{nr}\) by inverting the relation

\[
T_{ee} = f_Q (T_{nr}) T_{nr},
\]

where \(f_Q\) is the quenching factor, which is given in refs. [23, 83] for the CsI detector and in ref. [22] for the Ar detector.

An important characteristic of the neutrino beam in the COHERENT experiment is the time dependence of the neutrino flavor components: the prompt \(\nu_\mu\)’s produced in fast pion decay \((\tau_{\pi^+} \approx 26\) ns) arrive within about \(1\) \(\mu\)s from the on-beam trigger, whereas the delayed \(\nu_e\)’s and \(\bar{\nu}_\mu\)’s produced in the slower muon decay \((\tau_{\mu^+} \approx 2.2\) \(\mu\)s) arrive in a time interval which tails out at about \(10\) \(\mu\)s. Therefore, taking into account the time evolution of the data is useful for distinguishing the interactions of the two neutrino flavors. We implemented
the analyses of the COHERENT CsI and Ar data using the timing information provided by the COHERENT Collaboration [22, 23, 83] and distributing the theoretical CEνNS event numbers $N_{ij}^{\text{CEνNS}}$ in eq. (2.4) in time bins that are calculated from the exponential decay laws of the generating pions and muons. With this procedure we obtained the theoretical CEνNS event numbers $N_{ij}^{\text{CEνNS}}$, where $i$ is the index of the energy bins and $j$ is the index of the time bins.

We performed the analysis of the COHERENT CsI data in the energy and time bins considered in ref. [23]. Since in some energy-time bins the number of events is zero, we used the Poissonian least-squares function [84, 85]

$$\chi^2_{\text{CsI}} = 2 \sum_{i=1}^{9} \sum_{j=1}^{11} \sum_{z=1}^{4} \left( 1 + \eta_z \right) N_{ij}^{\text{exp}} \left( \frac{N_{ij}^{\text{exp}}}{\sum_{z=1}^{4} \left( 1 + \eta_z \right) N_{ij}^{\text{exp}}} \right) + \sum_{z=1}^{4} \left( \frac{\eta_z}{\sigma_z} \right)^2,$$

(2.6)

where the indices $i$ and $j$ denote, respectively, the energy and time bins, and the indices $z = 1, 2, 3, 4$ stand for CEνNS, beam-related neutron (BRN), neutrino-induced neutron (NIN), and steady-state (SS) backgrounds, respectively. In our notation, $N_{ij}^{\text{exp}}$ is the experimental event number obtained from coincidence (C) data, $N_{ij}^{\text{CEνNS}}$ is the predicted number of CEνNS events that depends on the physics model under consideration, $N_{ij}^{\text{BRN}}$ is the estimated BRN background, $N_{ij}^{\text{NIN}}$ is the estimated NIN background, and $N_{ij}^{\text{SS}}$ is the SS background obtained from the anti-coincidence (AC) data. We took into account the systematic uncertainties described in ref. [23] with the nuisance parameters $\eta_z$ and the corresponding uncertainties $\sigma_{\text{CEνNS}} = 0.12$ (which is the systematic uncertainty of the signal rate considering the effects of the 10%, 3.8%, 4.1%, and 3.4% uncertainties of the neutrino flux, quenching factor, CEνNS efficiency, and neutron form factors, respectively), $\sigma_{\text{BRN}} = 0.25$, $\sigma_{\text{NIN}} = 0.35$, and $\sigma_{\text{SS}} = 0.021$.

We performed the analysis of the COHERENT Ar data in the energy and time bins given in the data release [22] with the least-squares function

$$\chi^2_{\text{Ar}} = \sum_{i=1}^{12} \sum_{j=1}^{10} \left( N_{ij}^{\text{exp}} - \sum_{z=1}^{4} (1 + \eta_z + \sum_l \eta_{l,ij}^{\text{sys}}) N_{ij}^{\text{z}} \right)^2 \left( \frac{1}{\sigma_{ij}} \right)^2 + \sum_{z=1}^{4} \left( \frac{\eta_z}{\sigma_z} \right)^2 + \sum_{l, z} \left( \epsilon_{zl} \right)^2,$$

(2.7)

where $i$ is the index of the energy bins and $j$ is the index of the time bins. Here $z = 1, 2, 3, 4$ stands for the theoretical prediction of CEνNS, Steady-State (SS), Prompt Beam-Related Neutron (PBRN) and Delayed Beam-Related Neutron (DBRN) backgrounds, and $N_{ij}^{\text{exp}}$ is the number of observed events in each energy and time bin. The statistical uncertainty $\sigma_{ij}$ is given by

$$(\sigma_{ij})^2 = (\sigma_{ij}^{\text{exp}})^2 + (\sigma_{ij}^{\text{SS}})^2,$$

(2.8)

where $\sigma_{ij}^{\text{exp}} = \sqrt{N_{ij}^{\text{exp}}}$ and $\sigma_{ij}^{\text{SS}} = \sqrt{N_{ij}^{\text{SS}}/5}$. The factor 1/5 is due to the 5 times longer sampling time of the SS background with respect to the signal time window. The nuisance parameters $\eta_z$ quantify the systematic uncertainties of the event rate for the theoretical prediction of CEνNS, SS, PBRN, and DBRN backgrounds, with the corresponding uncertainties $\sigma_{\text{CEνNS}} = 0.13$, $\sigma_{\text{PBRN}} = 0.32$, $\sigma_{\text{DBRN}} = 1$, and $\sigma_{\text{SS}} = 0.0079$. We considered also the systematic uncertainties of the shapes of CEνNS and PBRN spectra using the
information in the COHERENT data release [22]. This is done in eq. (2.7) through the nuisance parameters $\epsilon_{zl}$ and the terms $\eta_{z_{l},ij}^{\text{sys}}$ given by

$$\eta_{z_{l},ij}^{\text{sys}} = \epsilon_{zl} \frac{N_{z_{l},ij}^{\text{sys}} - N_{z_{l},ij}^{\text{CV}}}{N_{z_{l},ij}^{\text{CV}}},$$

(2.9)

where $l$ is the index of the source of the systematic uncertainty. Here $N_{z_{l},ij}^{\text{sys}}$ and $N_{z_{l},ij}^{\text{CV}}$ are, respectively, $1\sigma$ probability distribution functions (PDFs) described in table 3 of ref. [22] and the central-value (CV) SM predictions described in table 2 of ref. [22]. For the theoretical prediction of CE$\nu$NS ($z = 1$), the sources of systematic shape uncertainties are the $F_{90}$ energy dependence and the mean time to trigger ($t_{\text{trig}}$) distribution. For the PBRN background ($z = 2$), the sources of systematic shape uncertainties are the energy, $t_{\text{trig}}$ mean, and $t_{\text{trig}}$ width distributions.

3 CE$\nu$NS process and light mediators

In the SM, the differential cross section as a function of the nuclear kinetic recoil energy $T_{nr}$ of the CE$\nu$NS process with a neutrino $\nu_\ell$ ($\ell = e, \mu, \tau$) and a nucleus $N$ is given by [86–88]

$$\frac{d\sigma_{\nu_\ell N}}{dT_{nr}}(E, T_{nr}) = \frac{G_F^2 M}{\pi} \left( 1 - \frac{M T_{nr}}{2E^2} \right) \left( Q_{\ell,SM}^V \right)^2,$$

(3.1)

where $G_F$ is the Fermi constant and

$$Q_{\ell,SM}^V = \left[ g_{V}^p (\nu_e) Z F_Z(|\vec{q}|^2) + g_{V}^n N F_N(|\vec{q}|^2) \right],$$

(3.2)

is the weak charge of the nucleus. Here, $Z$ and $N$ are the numbers of protons and neutrons in the nucleus, respectively, and $g_{V}^p$ and $g_{V}^n$ are the neutrino-proton and neutrino-neutron couplings, respectively. Taking into account radiative corrections in the $\overline{\text{MS}}$ scheme [89], accurate values of the vector couplings can be derived as [24]

$$g_{V}^p (\nu_e) = 0.0401, \quad g_{V}^p (\nu_\mu) = 0.0318, \quad g_{V}^n = -0.5094.$$

(3.3)

In eq. (3.2), $F_Z(|\vec{q}|^2)$ and $F_N(|\vec{q}|^2)$ are, respectively, the form factors of the proton and neutron distributions in the nucleus, which are the Fourier transforms of the corresponding nucleon distribution in the nucleus and describe the loss of coherence for large values of the momentum transfer $|\vec{q}|$. We use an analytic expression, namely the Helm parameterization [92], for the form factors, that gives practically equivalent results to the other two well known parameterizations, i.e., the symmetrized Fermi [93] and Klein-Nystrand [94] ones. The proton rms radii can be obtained from the muonic atom spectroscopy experiments [95, 96] as explained in ref. [24]

$$R_p(Cs) = 4.821 \text{ fm}, \quad R_p(I) = 4.766 \text{ fm}, \quad R_p(Ar) = 3.448 \text{ fm}.$$

(3.4)

\footnote{A different treatment of the hadronic uncertainties is discussed in refs. [90, 91]. The resulting small differences for the values of $g_{V}^p$ and $g_{V}^n$ can be neglected in the current analyses of CE$\nu$NS data which have other large uncertainties.}
On the other hand, there is a poor knowledge of the values of the $^{133}$Cs, $^{127}$I and $^{40}$Ar neutron rms radii obtained from the analyses of the COHERENT data [3, 4, 11, 13–15, 24, 97]. The values of these neutron rms radii can, however, be estimated with theoretical calculations based on different nuclear models [24, 27, 98]. Here, we consider the following values obtained from the recent nuclear shell model estimate of the corresponding neutron skins (i.e. the differences between the neutron and the proton rms radii) in ref. [98]

$$R_n(\text{Cs}) \simeq 5.09 \text{ fm}, \quad R_n(\text{I}) \simeq 5.03 \text{ fm}, \quad R_n(\text{Ar}) \simeq 3.55 \text{ fm}. \quad (3.5)$$

Following the COHERENT Collaboration [21–23], we take into account the effect of the uncertainty of the values of the neutron rms radii by considering 3.4% and 2% uncertainties for the CsI and Ar CE$\nu$NS rates, respectively.

The SM CE$\nu$NS differential event rates that are predicted for the COHERENT Ar and CsI detectors are shown in figure 1 as functions of $T_{nr}$. One can see that there are kinks at $T_{nr} \approx 50$ keV for Ar and $T_{nr} \approx 15$ keV for CsI. The steeper slope of the SM differential event rates below these values of $T_{nr}$ is due to the coherency condition $T_{nr} \lesssim 1/2MR^2$.

The CE$\nu$NS cross section is modified if there is a new massive mediator which couples to the SM leptons and quarks. In this work, we focus on two mediator types that have been considered in several previous works [6, 12, 14–16, 19, 25, 26, 70, 71, 99–108]: an additional vector mediator $Z'$ with mass $M_{Z'}$ associated to a new $U(1)'$ gauge group and an additional scalar mediator $\phi$ with mass $M_{\phi}$. The phenomenology of CE$\nu$NS in the specific models that we consider is briefly described in the following two subsections.

### 3.1 Light vector mediator

The interaction of a $Z'$ vector boson with neutrinos and quarks is described by the generic Lagrangian

$$\mathcal{L}^{V}_{Z'} = -Z'_\mu \left[ \sum_{\ell=e,\mu,\tau} g^{V}_{Z'} \bar{\nu}_\ell \gamma^\mu \nu_\ell \gamma^5 q + \sum_{q=u,d} g^{V}_{Z'} \bar{q} \gamma^\mu q \right], \quad (3.6)$$

where $g^{V}_{Z'}$ and $g^{V}_{Z'}$ are the couplings constants.

In the case of a vector mediator associated with a new $U(1)'$ gauge group, the coupling constants are proportional to the charges $Q'_q$ and $Q'_\ell$ of quarks and neutrinos under the new gauge symmetry: $g^{V}_{Z'} = g_{Z'} Q'_q$ and $g^{V}_{Z'} = g_{Z'} Q'_\ell$, where $g_{Z'}$ is the coupling constant of the symmetry group. Since both the SM and the $Z'$ interactions are of vector type, they contribute coherently to the CE$\nu$NS cross section. Moreover, since the vector current is conserved, the proton and neutron coupling are given by the sums of the couplings of their valence quarks. Therefore, the total cross section is obtained by replacing the SM weak charge $Q_{\ell,\text{SM}}$ with the new total weak charge (see appendix A)

$$Q_{\ell,\text{SM}+V} = Q_{\ell,\text{SM}} + \frac{g^{2}_{Z'} Q_{\ell}}{\sqrt{2}G_F (|q|^2 + M^2_{Z'})} \left[ (2Q'_u + Q'_d) ZF_Z (|q|^2) + (Q'_u + 2Q'_d) NF_N (|q|^2) \right], \quad (3.7)$$

with $|q|^2 \simeq 2MT_{nr}$. 

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\[
\begin{array}{|c|c|c|c|c|c|}
\hline
\text{Model} & Q'_u & Q'_d & Q'_e & Q'_\mu & Q'_\tau \\
\hline
\text{universal} & 1 & 1 & 1 & 1 & 1 \\
\hline
B - L & 1/3 & 1/3 & -1 & -1 & -1 \\
B - 3L_e & 1/3 & 1/3 & -3 & 0 & 0 \\
B - 3L_\mu & 1/3 & 1/3 & 0 & -3 & 0 \\
B - 2L_e - L_\mu & 1/3 & 1/3 & -2 & -1 & 0 \\
B - L_e - 2L_\mu & 1/3 & 1/3 & -1 & -2 & 0 \\
B_y + L_\mu + L_\tau & 1/3 & 1/3 & 0 & 1 & 1 \\
\hline
L_e - L_\mu & 0 & 0 & 1 & -1 & 0 \\
L_e - L_\tau & 0 & 0 & 1 & 0 & -1 \\
L_\mu - L_\tau & 0 & 0 & 0 & 1 & -1 \\
\hline
\end{array}
\]

Table 1. The U(1)' charges of quarks and leptons in the vector mediator models considered in this work.

In this work we consider the models listed in table 1. There are many models beyond the SM with an additional massive Z' vector boson associated with a new U(1)' gauge symmetry (see, e.g., the review in ref. [69]). A necessary requirement is that the theory is anomaly-free. However, it is possible to consider effective anomalous models that describe the interactions of SM fermions with the implicit requirement that the anomalies are canceled by the contributions of the non-standard fermions of the full theory. This is the case of the first model that we consider: a Z' boson which couples universally to all SM fermions [6, 12, 14, 15, 26, 70, 71]. In this case \(Q'_e = Q'_u = Q'_d = 1\), and the coupling is same for all the fermions.

Other models that we consider are anomaly-free if the SM is extended with the introduction of three right-handed neutrinos (see, e.g., ref. [109]), which are also beneficial for the generation of the neutrino masses that are necessary for the explanation of the oscillations of neutrinos observed in many experiments (see, e.g., refs. [85, 110]). In this case, there is an infinite set of anomaly-free U(1)' gauge groups generated by

\[
G(c_1, c_2, c_3, c_e, c_\mu, c_\tau) = c_1B_1 + c_2B_2 + c_3B_3 - c_eL_e - c_\mu L_\mu - c_\tau L_\tau,
\]

where \(B_1, B_2, \text{and} B_3\) are the baryon numbers of the three generations and \(L_\alpha\) are the lepton numbers for \(\alpha = e, \mu, \tau\). We assume that for each generation the U(1)' couplings of the right-handed neutrino is the same as that of the left-handed neutrino in order to have vectorial U(1)' interactions. Therefore, when we extend the SM gauge group \(SU(3)_C \times SU(2)_L \times U(1)_Y\) to \(SU(3)_C \times SU(2)_L \times U(1)_Y \times U(1)'\), there are no \([SU(3)_C]^2U(1)_Y\), \([U(1)']^3\) and \([\text{gravity}]^2U(1)'\) anomalies, because of the vectorial character of the involved interactions. The \([U(1)']^2U(1)_Y\) anomaly cancels because for each generation the difference
of the $Y$ charges of left-handed and right-handed quarks (leptons) is zero. The remaining $[SU(2)_L]^2U(1)'$ and $[U(1)_Y]^2U(1)'$ anomalies are canceled with the constraint

$$c_1 + c_2 + c_3 - c_e - c_\mu - c_\tau = 0. \quad (3.9)$$

It is often assumed that the quark charges are universal, in order to avoid unobserved flavor-changing neutral currents in the quark sector. In this case, we have

$$G_B(c_B, c_e, c_\mu, c_\tau) = c_B B - c_e L_e - c_\mu L_\mu - c_\tau L_\tau, \quad (3.10)$$

with the constraint (see, e.g., refs. [111, 112])

$$3c_B - c_e - c_\mu - c_\tau = 0. \quad (3.11)$$

Here $B = B_1 + B_2 + B_3$ is the usual baryon number.

We consider the following anomaly-free models that correspond to different choices of the coefficients in eq. (3.8) or (3.10) and contribute to CE$\nu$NS interactions of $\nu_e$ and $\nu_\mu$:

$\mathcal{B} - \mathcal{L} = G_B(1, 1, 1, 1)$. Here $L = L_e + L_\mu + L_\tau$ is the total lepton number. This is the most popular $Z'$ model, with a huge literature (see, e.g., the reviews in refs. [69, 72, 73]). It was considered recently in several CE$\nu$NS phenomenological analyses, e.g. those in refs. [25, 26, 71, 104, 113]. Note that, since there are no $\nu_\tau$'s in the COHERENT neutrino beam, bounds on the coupling constant in the anomaly-free model generated by

$$G_B(1, 3/2, 3/2, 0) = B - \frac{3}{2} (L_e + L_\mu), \quad (3.12)$$

considered, e.g., in ref. [102], can be obtained from the bounds on the coupling constant $g_{Z'}$ in the $\mathcal{B} - \mathcal{L}$ model by rescaling it by the factor $\sqrt{2/3}$, because the $\nu_e$ and $\nu_\mu$ couplings are changed by the same factor $3/2$.

$\mathcal{B}_y + \mathcal{L}_\mu + \mathcal{L}_\tau = G(1, -y, y - 3, 0, -1, -1)$. In this model, proposed in ref. [114] and considered, e.g., in ref. [113], $\mathcal{B}_y = B_1 - yB_2 + (y - 3)B_3$.

$\mathcal{B} - 3\mathcal{L}_e = G_B(1, 3, 0, 0)$. This model was considered, e.g., in refs. [102, 104, 113, 115]. In this case, only the $\nu_e$ CE$\nu$NS cross section is affected by the new $Z'$-mediated interaction. Moreover, since there are no $\nu_\tau$'s in the COHERENT neutrino beam, the bounds on the coupling constant $g_{Z'}$ obtained in this model can be extended to all the anomaly-free models generated by

$$G_B(1, 3w_e, 0, 3(1 - w_e)) = B - 3w_e L_e - 3(1 - w_e) L_\tau \quad (3.13)$$

through a rescaling of the coupling constant by a factor $1/\sqrt{w_e}$.

$\mathcal{B} - 3\mathcal{L}_\mu = G_B(1, 0, 3, 0)$. This model was considered, e.g., in refs. [104, 113, 115]. In this case, only the $\nu_\mu$ CE$\nu$NS cross section is affected by the new $Z'$-mediated interaction and, in analogy with the argument in the previous item, the bounds on the coupling
constant \( g_{Z'} \), obtained in this model can be extended to all the anomaly-free models generated by

\[
G_B(1, 0, 3w_\mu, 3(1 - w_\mu)) = B - 3w_\mu L_\mu - 3(1 - w_\mu)L_{\tau} \tag{3.14}
\]

through a rescaling of the coupling constant by a factor \( 1/\sqrt{\bar{w}_1} \). For example, the \( B - (3/2)(L_\mu + L_{\tau}) \) considered in refs. \cite{113, 115} is obtained with \( \bar{w}_1 = 1/2 \).

**B - 2L_e - L_\mu = G_B(1, 2, 1, 0).** This model was considered, e.g., in ref. \cite{104}. In analogy with the discussion in the previous items, the bounds on the coupling constant \( g_{Z'} \), obtained in this model can be extended to all the anomaly-free models generated by

\[
G_B(1, 2w_1, w_1, 3(1 - w_1)) = B - 2w_1L_e - w_1 L_\mu - 3(1 - w_1)L_{\tau} \tag{3.15}
\]

through a rescaling of the coupling constant by a factor \( 1/\sqrt{\bar{w}_1} \).

**B - L_e - 2L_\mu = G_B(1, 1, 2, 0).** This model, was considered, e.g., in ref. \cite{104}. Again, in analogy with the discussion in the previous items, the bounds on the coupling constant \( g_{Z'} \), obtained in this model can be extended to all the anomaly-free models generated by

\[
G_B(1, w_2, 2w_2, 3(1 - w_2)) = B - w_2L_e - 2w_2 L_\mu - 3(1 - w_2)L_{\tau} \tag{3.16}
\]

through a rescaling of the coupling constant by a factor \( 1/\sqrt{\bar{w}_2} \).

The effects of the models above on the CEνNS differential event rates that are predicted for the COHERENT Ar and CsI detectors are illustrated, respectively, in figures 1a and 1b. In these figures we choose \( g_{Z'} = 10^{-4} \) and \( M_{Z'} = 10 \text{ MeV} \) and we compared the model predictions with the SM one. One can see that the effects of the light mediator are similar for the Ar and CsI detectors and the vector boson mediator contribution increases for small values of \( T_{\text{nr}} \simeq |\bar{q}|^2/2M \) because of the propagator in eq. (3.7). The different scales of \( T_{\text{nr}} \) in figures 1a and 1b are obviously due to the different masses of the nuclei.

In the case of the universal \( Z' \) model there is a deep dip due to a cancellation between the negative SM and the positive \( Z' \) contributions to the weak charge in eq. (3.7). This occurs only in the universal model because only in this case all the quark and lepton charges are positive and both \( \nu_e \) and \( \nu_\mu \) interact with the \( Z' \). Indeed, there is a cancellation for

\[
T_{\text{nr}} = - \frac{1}{2M} \left( \frac{3g_{Z'}^2}{\sqrt{2}G_F} \frac{ZF_Z(|\bar{q}|^2) + NF_N(|\bar{q}|^2)}{g_{Z'}^p ZF_Z(|\bar{q}|^2) + g_{Z'}^N NF_N(|\bar{q}|^2) + M_{Z'}^2} \right), \tag{3.17}
\]

which occurs at \( T_{\text{nr}} \approx 92 \text{ keV} \) for Ar in figure 1a and \( T_{\text{nr}} \approx 27 \text{ keV} \) for CsI in figure 1b.

There is a cancellation for \( \nu_\mu \) also in the \( B_\mu + L_\mu + L_{\tau} \) model, since the quarks and \( \nu_\mu \) have positive charges (see table 1). The cancellation occurs at

\[
T_{\text{nr}} = - \frac{1}{2M} \left( \frac{g_{Z'}^2}{\sqrt{2}G_F} \frac{ZF_Z(|\bar{q}|^2) + NF_N(|\bar{q}|^2)}{g_{Z'}^p ZF_Z(|\bar{q}|^2) + g_{Z'}^N NF_N(|\bar{q}|^2) + M_{Z'}^2} \right), \tag{3.18}
\]
Figure 1. Predicted CEνNS differential event rates corresponding to the experimental configuration and data taking time of the COHERENT Ar (a, c) and CsI (b, d) detectors in the vector mediator models considered in this work.

which corresponds to $T_{\text{nr}} \simeq 29$ keV for Ar in figure 1a and $T_{\text{nr}} \simeq 8$ keV for CsI in figure 1b. Since in this case there is no cancellation of the SM contribution of $\nu_e$, which does not interact with the $Z'$, there are only shallow dips at these energies in figures 1a and 1b for this model. Note that the total differential rate is smaller than the SM differential rate for energies above the dip, because the positive and smaller $Z'$ contribution to $Q_{\mu, \text{SM} + V}$ is added to the dominant negative SM contribution, decreasing the absolute value of $Q_{\mu, \text{SM} + V}$.

In all the other models above the quarks and leptons have opposite charges (see table 1) and the $Z'$ contribution to the weak charge in eq. (3.7) is negative as the SM contribution. Therefore, the total differential rate is larger than the SM rate for all values of $T_{\text{nr}}$, as shown in figures 1a and 1b.
We also consider the following three possible $L_\alpha - L_\beta$ models that are anomaly-free and can be gauged without extending the SM content with right-handed neutrinos [74–77]:

$L_e - L_\mu = G_B(0, -1, 1, 0)$. This model, obtained from eq. (3.10) with $c_B = 0$, $c_e = -1$ $c_\mu = 1$, and $c_\tau = 0$, was considered, e.g., in refs. [76, 113, 116].

$L_e - L_\tau = G_B(0, -1, 0, 1)$. This model, obtained from eq. (3.10) with $c_B = 0$, $c_e = -1$ $c_\mu = 0$, and $c_\tau = 1$, was considered, e.g., in refs. [76, 113, 116].

$L_\mu - L_\tau = G_B(0, 0, -1, 1)$. This model, obtained from eq. (3.10) with $c_B = 0$, $c_\tau = 0$ $c_\mu = -1$, and $c_\tau = 1$, was considered in many papers, e.g., in refs. [26, 28, 59, 71, 76, 78, 79, 117].

Since in these models the $Z'$ vector boson does not couple to quarks, there are no tree-level interactions that contribute to CE$\nu$NS (assuming the absence of tree-level kinetic mixing). However, there is kinetic mixing of the $Z'$ and the photon at the one-loop level that induces a contribution to CE$\nu$NS through the photon interaction with quarks [28, 78, 79]. The CE$\nu$NS cross section in these three models is [26, 78]$^2$

$$\left( \frac{d\sigma}{dT_{nr}} \right)_{L_\alpha - L_\beta}^{\nu_\tau - N} (E, T_{nr}) = \frac{G_F^2 M}{\pi} \left( 1 - \frac{MT_{nr}}{2E^2} \right)$$

$$\times \left\{ \bar{g}_\nu^2 (\mu_\ell) + \frac{\sqrt{2} \alpha_{EM} g_Z^2 (\delta_{\ell\alpha} \varepsilon_{\beta\alpha} (|q|) + \delta_{\ell\beta} \varepsilon_{\alpha\beta} (|q|))}{\pi G_F (|q|^2 + M_{Z'}^2)} \right\}^2 ZF_2 (|q|^2) + g_\ell^0 N F_{\nu \tau} (|q|^2),$$

where $\alpha_{EM}$ is the electromagnetic fine-structure constant and $\varepsilon_{\beta\alpha} (|q|)$ is the one-loop kinetic mixing coupling, that is given by [28, 79]

$$\varepsilon_{\beta\alpha} (|q|) = \int_0^1 x (1 - x) \ln \left( \frac{m_\beta^2 + x(1 - x) |q|^2}{m_\alpha^2 + x(1 - x) |q|^2} \right) dx,$$  

(3.20)

where $m_\beta$ and $m_\alpha$ are the charged lepton masses and we took into account that for CE$\nu$NS $q^2 \approx -|q|^2 \approx -2MT_{nr}$. Note that the $Z'$ contribution is invariant for $\alpha \leftrightarrow \beta$, as it should be, since $L_\alpha - L_\beta$ and $L_\beta - L_\alpha$ are physically equivalent. Note also that the sign of the loop contribution of the $i$ charged lepton to $\nu_\tau$ scattering is given by $-Q_i^\prime Q_{\ell i}^\prime$, where the minus comes from the negative electric charge of the charged lepton propagating in the loop. Therefore, the mass of the charged lepton with the same flavor $\ell$ of the scattering neutrino is always at the denominator of the logarithm in eq. (3.20) and the mass of the other charged lepton taking part to the new symmetry is always at the numerator. Figure 2 shows the value of $\varepsilon_{\beta\alpha} (|q|)$ for each of the three $L_\alpha - L_\beta$ symmetries as a function of $|q|$ in the range of the COHERENT CE$\nu$NS. One can see that only $\varepsilon_{\tau\mu}$ is almost constant, because $|q| \ll m_\tau$ and $|q| < m_\mu$. In this case it is possible to approximate $\varepsilon_{\tau\mu} \approx \ln(m_\tau^2/m_\mu^2)/6$, as done in refs. [26, 71, 78]. On the other hand, for the symmetries $L_e - L_\mu$ and $L_e - L_\tau$ the $|q|$ dependence of $\varepsilon_{\beta\alpha}$ on $|q|$ must be taken into account, because $|q| \gg m_e$.

$^2$We correct here the sign of the $Z'$ contribution with respect to that used in ref. [26]. Let us also note that in the analysis in ref. [28] the $Z'$ contribution has the correct sign, but there is an additional factor 1/2 that is incorrect, as shown in appendix A.
Figure 2. Values of $\varepsilon_{\beta\alpha}$ in eq. (3.20) for each of the three $L_\alpha - L_\beta$ symmetries as a function of $q = |\vec{q}| \simeq \sqrt{2 MT_{nr}}$ in the range of the COHERENT CE$\nu$NS data.

Figures 1c and 1d illustrate the effects of the $Z'$ contribution to the CE$\nu$NS differential event rates that are predicted for the COHERENT Ar and CsI detectors in the $L_\alpha - L_\beta$ models. In these figures we choose $g_{Z'} = 2 \times 10^{-3}$ and $M_{Z'} = 10$ MeV and we compared the model predictions with that of the SM. One can see that, as for the models in figures 1a and 1b discussed above, the effects of the light mediator are similar for the Ar and CsI detectors and the vector boson mediator contribution increases for small values of $T_{nr} \simeq |\vec{q}|^2/2M$ because of the propagator in eq. (3.7).

In the case of the $L_\mu - L_\tau$ model the $Z'$ contribution to $Q_{\mu,SM+V}^V$ is positive and there can be a cancellation with the negative SM contribution. The cancellation occurs at

$$T_{nr} = -\frac{1}{2M} \left( \frac{\alpha_{EM} g_{Z'}^2}{3\pi \sqrt{2} G_F} \ln \left( \frac{m_\tau^2}{m_\mu^2} \right) \frac{ZF_2(|\vec{q}|^2)}{g_\nu^V ZF_2(|\vec{q}|^2) + g_\nu^N F_2(|\vec{q}|^2) + M_{Z'}^2} \right),$$

(3.21)

which corresponds to $T_{nr} \simeq 23$ keV for Ar in figure 1c and $T_{nr} \simeq 6$ keV for CsI in figure 1d. Since there is no cancellation of the SM contribution of $\nu_e$, which does not interact with the $Z'$, there are only shallow dips at these energies in figures 1c and 1d for this model. The total differential rate is smaller than the SM differential rate for energies above the dip for the same reason that has been discussed above for the $B_y + L_\mu + L_\tau$ model.

In the case of the $L_e - L_\tau$ model, there can be a cancellation of the positive $Z'$ contribution to $Q_{e,SM+V}^V$ with the negative SM contribution, but it is difficult to estimate for which value of $T_{nr}$ because of the strong dependence of $\varepsilon_{\tau e}$ on $T_{nr} \simeq |\vec{q}|^2/2M$ shown in figure 2. However, one can see from figures 1c and 1d that there are shallow dips of the differential rates at values of $T_{nr}$ that are larger than in the $L_\mu - L_\tau$ model, because $\varepsilon_{\tau e} > \varepsilon_{\tau \mu}$, as shown in figure 2. The dip is more shallow than in the $L_\mu - L_\tau$ model because the $\nu_e$ contribution to the CE$\nu$NS event rate is smaller than the sum of the $\nu_\mu$ and $\bar{\nu}_\mu$ contributions.
Figure 3. Predicted CE$\nu$NS differential event rates corresponding to the experimental configuration and data taking time of the COHERENT Ar (a) and CsI (b) detectors in the universal scalar mediator model.

In the case of the $L_e - L_\mu$ model, the situation is more complicated, because the $Z'$ contribution to $Q_{e,SM+V}^V$ is positive, since $\varepsilon_{e\mu} > 0$, but the $Z'$ contribution to $Q_{\mu,SM+V}^V$ is negative, since $\varepsilon_{\mu e} < 0$. Therefore, the $Z'$ contributions of the dominant $\nu_\mu$ and $\bar{\nu}_\mu$ fluxes enhance the CE$\nu$NS differential event rate with respect to the SM prediction, whereas the subdominant $\nu_e$ flux generate a decrease for sufficiently large values of $T_{\text{nr}}$ (about 40 keV for Ar in figure 1c and 15 keV for CsI in figure 1d). As a result of these opposite contributions, the total CE$\nu$NS differential rates of the $L_e - L_\mu$ model shown in figures 1c and 1d are only slightly larger than the SM rates in the large-$T_{\text{nr}}$ parts of the figures.

3.2 Light scalar mediator

Non-standard neutrino interactions mediated by a scalar boson $\phi$ are possible if the SM fermion content is extended with the addition of right-handed neutrinos. The generic Lagrangian that describes the interaction of $\phi$ with neutrinos and quarks is

$$L^S_{\phi} = -\phi \left[ \sum_{\ell=e,\mu,\tau} g^\nu_\ell \overline{\nu_\ell} \nu_\ell + \sum_{q=u,d} g^q_\phi \overline{q} q \right],$$

where $\nu_\ell = \nu_{\ell L} + \nu_{\ell R}$ and $g^\nu_\ell$ and $g^q_\phi$ are the coupling constants. The contribution of the scalar boson interaction to the CE$\nu$NS cross section adds incoherently to the SM cross section \cite{7, 10, 80–82}

$$\frac{d\sigma_{\nu e,N}}{dT_{\text{nr}}} = \left( \frac{d\sigma_{\nu e,N}}{dT_{\text{nr}}} \right)_\text{SM} + \left( \frac{d\sigma_{\nu e,N}}{dT_{\text{nr}}} \right)_\text{scalar},$$

with

$$\left( \frac{d\sigma_{\nu e,N}}{dT_{\text{nr}}} \right)_\text{scalar} = \frac{M^2 T_{\text{nr}}}{4\pi E^2} \frac{(g^\nu_\ell)^2 Q_\phi^2}{(|q|^2 + M^2_\phi)}.$$
where $Q_\phi$ is the scalar charge of the nucleus, given by

$$Q_\phi = ZF_Z(|q|^2) \sum_{q=u,d} g_\phi^q \langle p|\bar{q}q|p \rangle + NF_N(|q|^2) \sum_{q=u,d} g_\phi^q \langle n|\bar{q}q|n \rangle. \quad (3.25)$$

It is sometimes written as [10, 80–82]

$$Q_\phi = ZF_Z(|q|^2) \sum_{q=u,d} g_\phi^q \frac{m_q}{m_q} f_q^q + NF_N(|q|^2) \sum_{q=u,d} g_\phi^q \frac{m_q}{m_q} f_q^m. \quad (3.26)$$

with the quark contributions to the nucleon masses

$$f_q^N = \frac{m_q}{m_n} \langle N|\bar{q}q|N \rangle, \quad (3.27)$$

for $N = p, n$. Since the scalar currents are not conserved, the scalar charges of the nucleons are not simply given by the sums of the charges of their valence quarks, as in the case of a vector boson mediator (see eq. (3.7)). The proton and neutron matrix elements of the scalar quark current must be calculated (see, e.g., the recent refs. [118–121]). For simplicity, we consider equal couplings for the $u$ and $d$ quarks and equal couplings for $\nu_e$ and $\nu_\mu$

$$g_\phi^u = g_\phi^d = g_\phi^q \quad \text{and} \quad g_\phi^{\nu_e} = g_\phi^{\nu_\mu}. \quad (3.28)$$

Then, we have

$$Q_\phi = g_\phi^q \left[ ZF_Z(|q|^2) \langle p|\bar{u}u + \bar{d}d|p \rangle + NF_N(|q|^2) \langle n|\bar{u}u + \bar{d}d|n \rangle \right]. \quad (3.29)$$

Considering the isospin approximation, we obtain

$$\langle p|\bar{u}u + \bar{d}d|p \rangle = \langle n|\bar{u}u + \bar{d}d|n \rangle = \langle N|\bar{u}u + \bar{d}d|N \rangle = \frac{\sigma_{\pi N}}{m_{ud}}, \quad (3.30)$$

where $m_{ud} = (m_u + m_d)/2$ and $\sigma_{\pi N}$ is the pion-nucleon $\sigma$-term that has been determined in different ways in the literature (see the recent review in ref. [122]). Recent values have been obtained from pionic atoms and pion-nucleon scattering [118, 123, 124] and from lattice calculations [119, 121]. Since there are large uncertainties on the values of $\sigma_{\pi N}$ and $m_{ud}$, we choose a reference value for $\sigma_{\pi N}/m_{ud}$ given by the ratio of the central value of $\sigma_{\pi N}$ determined in ref. [118] ($\sigma_{\pi N} = 59.1 \text{ MeV}$) and the central PDG values [85] $m_u = 2.16 \text{ MeV}$ $m_d = 4.67 \text{ MeV}$, that gives

$$\left( \frac{\sigma_{\pi N}}{m_{ud}} \right)_{\text{ref}} = 17.3, \quad (3.31)$$

that allows us to write the scalar cross section (3.24) as

$$\left( \frac{d\sigma_{\nu_e\pi^{-}}}{dT_{\nu_e\pi^{-}}} \right)_{\text{scalar}} = \frac{M^2 T_{\nu_e}}{4\pi E^2} \frac{g_\phi^4}{(g_\phi^4 + M^2)^2} \left( \frac{\sigma_{\pi N}}{m_{ud}} \right)_{\text{ref}}^2 \left[ ZF_Z(|q|^2) + NF_N(|q|^2) \right]^2, \quad (3.32)$$

with

$$\tilde{g}_\phi^2 = g_\phi^{\nu_e} g_\phi^{\nu_\mu} \frac{\sigma_{\pi N}/m_{ud}}{(\sigma_{\pi N}/m_{ud})_{\text{ref}}}. \quad (3.33)$$

---

\textsuperscript{3}We neglect the small $|q|$-dependent corrections discussed in ref. [98].
In this way the results of other calculations can be compared with our results by appropriate rescaling of $\tilde{g}_\phi$ according with the assumptions. We guess that $\tilde{g}_\phi$ is practically equal to $g_\phi$ in ref. [25], where the expression (3.26) was used for the scalar charge of the nucleus, with the values of the $f_N^q$'s given in ref. [118], although the assumed values of the quark masses are not specified. Indeed, the values of the $f_N^q$'s in ref. [118] have been obtained from the value of $\sigma_{\pi N}$ using eq. (13) of ref. [125], which implies

$$\sum_{q=u,d} \frac{m_p}{m_q} f^p_q = \sum_{q=u,d} \frac{m_n}{m_q} f^n_q = \frac{\sigma_{\pi N}}{m_{ud}}. \quad (3.34)$$

On the other hand, our approach is different from that in refs. [15, 80, 126], which considered different values for the proton and neutron matrix elements in eq. (3.29):

$$\langle p|\bar{u}u + \bar{d}d|p\rangle = 15.1 \quad \text{and} \quad \langle n|\bar{u}u + \bar{d}d|n\rangle = 14.\quad \text{These values correspond to a rather large 8\% violation of the isospin symmetry.}$$

Let us also note that our treatment neglected the contribution of the strange and heavier quarks, whose contributions to the nucleon mass have very large uncertainties (see, e.g., table 4 of ref. [127]). If one wants to consider them, their contributions can be taken into account by rescaling appropriately $\tilde{g}_\phi$, assuming that the coupling of $\phi$ with all quarks is the same.

Figure 3 illustrates the effect of the scalar boson mediator on the CE$\nu$NS differential event rates that are predicted for the COHERENT Ar and CsI detectors for $\tilde{g}_\phi = 10^{-4}$ and $M_\phi = 50$ MeV. One can see that the total CE$\nu$NS rates are larger than the SM rates for all values of $T_{nr}$, because the scalar boson cross section adds incoherently to the SM cross section, according to eq. (3.23). In the two panels of figure 3 one can also notice that the total CE$\nu$NS rates represented by the red-dashed lines have small discontinuities at $T_{nr} = 47.7$ keV for Ar and $T_{nr} \approx 15$ keV for CsI. These values correspond to the maximum nuclear kinetic energy $T_{nr}^{\text{max}} = 2E^2/M$ for the monoenergetic $\nu_\mu$ from pion decay ($E = 29.8$ MeV), as shown by the green-dashed lines that represent the $\nu_\mu$ contributions. One can see that there is an effect also for the SM differential event rates, which change slope at the same values of $T_{nr}$. The effect for the scalar boson contribution is larger because it is enhanced by the $T_{nr}$ in the numerator of the scalar cross section, see eq. (3.24). Such a dependence causes also the decrease of the scalar contribution for very low values of $T_{nr}$ that is visible in figure 3.

4 Constraints on light mediator models

In this section we present the results of the analyses of the COHERENT CsI and Ar data with the light-mediator models described in section 3. Since the data are fitted well by the SM CE$\nu$NS prediction, we obtain constraints on the mass and coupling of the light mediator in each model. Let us note that the constraints that can be obtained with previous COHERENT CsI and Ar data have been presented in refs. [6, 9, 16, 19, 26, 28] for the more popular universal, $B - L$, and $L_\mu - L_\tau$ models and in ref. [113] for the $B - 3L_e$, $B - 3L_\mu$, and $B_\mu + L_\mu + L_\tau$ models.

In the following subsections, we present the 2$\sigma$ (95.45% C.L.) limits obtained from the COHERENT Ar and CsI data for the models discussed in section 3 and we compare...
Figure 4. Excluded regions (2σ) in the $M_{Z'}-g_{Z'}$ plane for the universal vector mediator model.

them with the constraints of other experiments by using the darkcast [128] code for re-casting the limits in the different models under consideration. In particular, we compare the constraints on the light vector boson mediator obtained from the COHERENT data with the excluded regions obtained from searches of visible dark photon decays in beam dump (E141 [129], E137 [130], E774 [131], KEK [132], Orsay [133–135], ν-CAL I [136–139], CHARM [140, 141], NOMAD [142], and PS191 [143, 144]), fixed target (A1 [145] and APEX [146]), collider (BaBar [147], KLOE [148, 149], LHCb [150]), and rare-meson-decay (NA48/2 [151]) experiments, and searches of invisible dark photons decays in the NA64 [152] and BaBar [153] experiments. We also compare the constraints with the excluded regions obtained from the global analysis of oscillation data (OSC) [113].

4.1 Universal $Z'$ model

Figure 4 shows the 2σ limits that we obtained from the COHERENT Ar and CsI data for the universal $Z'$ model [6, 12, 14, 15, 26, 70, 71]. The black line delimits the 2σ allowed regions obtained from the combined analysis of the CsI and Ar data, while the blue and red lines delimit the excluded regions obtained from the CsI and Ar data, respectively.

Considering the combined analysis of the CsI and Ar data, one can see that in the low-mass region the black line, which represents the upper boundary of the 2σ allowed region, flattens due to the fact that the contribution of the $Z'$ boson to $Q_{V,SM+V}$ is small. This happens for $M_{Z'} \ll 100$ MeV, because $g_{Z'}$ is small and the boundary does not depend on $M_{Z'}$ since $|\vec{q}| \gg M_{Z'}$ in the $Z'$ boson propagator. On the other hand, for higher masses the contribution of the $Z'$ boson is suppressed by a large $M_{Z'}$, which is dominant in the propagator, and the boundary is given by a diagonal line proportional to $M_{Z'}$. The numerical values of the 2σ limits in these two simple cases are given in table 2.

In the upper-middle part of figure 4, one can see that another black line delimits a thin diagonal strip, where $Q_{V,SM+V}^V \simeq -Q_{SM}^V$, corresponding to a degeneracy with the SM
cross section, as explained in ref. [26]. Neglecting the form factors and the small proton SM contribution, one can find that the thin allowed strip corresponds to

$$
(g_{Z'}^{\text{univ}})_{\text{strip}} \simeq \sqrt{\frac{N}{A}} \frac{\sqrt{2} G_F M_{Z'}^2}{3} \simeq 1.8 \times 10^{-3} \frac{M_{Z'}}{\text{GeV}},
$$

(4.1)

taking into account that \((N/A)_{\text{Ar}} \simeq (N/A)_{\text{CsI}} \simeq 0.58\). Note that the existence of the allowed strip in the universal model is related to the possibility to have a cancellation of the CE+NS differential event rate discussed in section 3 (see eq. (3.17)) because it is a consequence of the different signs of the SM and \(Z\) contributions to \(Q_{\text{univ}}^{\text{SM}+\text{V}}\). Indeed, all the models that can have a cancellation of the CE+NS differential as discussed in section 3 (i.e. the universal, \(B_y + L_{\mu} + L_{\tau}, L_e - L_{\tau}\)), and \(L_{\mu} - L_{\tau}\) models) have an allowed strip, as discussed in the following. The cancellation occurs in the excluded parameter space between the lower allowed region and the thin allowed strip for

$$
(g_{Z'}^{\text{univ}})_{\text{canc}} \simeq \sqrt{\frac{N}{A}} \frac{\sqrt{2} G_F M_{Z'}^2}{6} \simeq 1.3 \times 10^{-3} \frac{M_{Z'}}{\text{GeV}},
$$

(4.2)

where we neglected the form factors and the small proton SM contribution.

One can see from figure 4 that the limits obtained from the CsI data are stricter than those obtained from the Ar data and are close to those of the combined fit. The limits obtained from the analysis of the Ar data are more complicated and one can see that there

| model            | \(g_{Z'}(\text{low } M_{Z'})\) | \(g_{Z'}(\text{high } M_{Z'})\) | \(g_{Z'}(\text{low } M_{Z'})\) | \(g_{Z'}(\text{high } M_{Z'})\) |
|------------------|-------------------------------|-------------------------------|-------------------------------|-------------------------------|
| universal        | \(3.91 \times 10^{-5}\)       | \(0.82 \times 10^{-3}\)       | \(2.36 \times 10^{-5}\)       | \(0.53 \times 10^{-3}\)       |
| \(B - L\)        | \(5.35 \times 10^{-5}\)       | \(1.67 \times 10^{-3}\)       | \(5.27 \times 10^{-5}\)       | \(1.00 \times 10^{-3}\)       |
| \(B - 3L_{\mu}\) | \(10.4 \times 10^{-5}\)       | \(3.58 \times 10^{-3}\)       | \(4.97 \times 10^{-5}\)       | \(1.14 \times 10^{-3}\)       |
| \(B - 3L_{\tau}\) | \(4.91 \times 10^{-5}\)       | \(1.55 \times 10^{-3}\)       | \(5.16 \times 10^{-5}\)       | \(0.96 \times 10^{-3}\)       |
| \(B - 2L_{e} - L_{\mu}\) | \(3.45 \times 10^{-5}\) | \(1.09 \times 10^{-3}\)       | \(3.21 \times 10^{-5}\)       | \(0.64 \times 10^{-3}\)       |
| \(B - L_{e} - L_{\mu}\) | \(4.62 \times 10^{-5}\)       | \(1.48 \times 10^{-3}\)       | \(4.79 \times 10^{-5}\)       | \(0.89 \times 10^{-3}\)       |
| scalar           | \(3.97 \times 10^{-5}\)       | \(1.28 \times 10^{-3}\)       | \(3.86 \times 10^{-5}\)       | \(0.75 \times 10^{-3}\)       |

Table 2. The 2\(\sigma\) (95.45\% C.L.) upper bounds on the coupling of the new boson mediator obtained from the separate and combined analyses of the Ar and CsI COHERENT CE+NS data for low and high values of the boson mass in the models considered in this paper. \(g_{Z'}/M_{Z'}\) and \(\tilde{g}_{\phi}/M_{\phi}\) are in units of GeV\(^{-1}\).
are three corresponding red dashed lines in figure 4. The lowest one represents the upper boundary of the 2σ allowed region where the contribution of the $Z'$ boson to $Q_{\ell, SM+V}^V$ is small, similarly to the blue-dashed line below and the black line further below that correspond to the CsI fit and the combined fit, respectively. The two red-dashed lines above delimit the strip in which the Ar data are well-fitted $Q_{\ell, SM+V}^V \approx -Q_{SM}^V$, as discussed above for the combined fit. However, since the Ar data are less constraining, the strip is wider than those obtained from the CsI and combined analyses and it extends to small values of $M_{Z'}$.

In figure 4 we compared the limits obtained from the COHERENT CE$\nu$NS data with those of non-CE$\nu$NS experiments and those of the CONNIE reactor CE$\nu$NS experiment [154]. Figure 4 shows also the $(g - 2)_\mu$ 2σ allowed band which can explain the anomalous magnetic moment of the muon in this model [56, 68] (see appendix B). One can see that the explanation of the $(g - 2)_\mu$ anomaly with the universal model is excluded by the combination of the non-CE$\nu$NS exclusion limits in figure 4, by the CONNIE CE$\nu$NS bounds alone, and by the COHERENT CE$\nu$NS limits alone, which confirm and extend the CONNIE CE$\nu$NS bounds. Moreover, the COHERENT CE$\nu$NS limits extend the total exclusion region by covering a previously not-excluded area for $20 \text{ MeV} \lesssim M_{Z'} \lesssim 200 \text{ MeV}$ and $2 \times 10^{-5} \lesssim g_{Z'} \lesssim 10^{-4}$. The new COHERENT CE$\nu$NS limits are consistent with those obtained in ref. [26] using the first COHERENT CsI data and slightly extend the COHERENT CE$\nu$NS exclusion region.

### 4.2 $B - L$ model

The gauged $B - L$ model is the most popular $Z'$ model (see, e.g., the reviews in refs. [69, 72, 73]) and its effects in CE$\nu$NS have been studied in refs. [25, 26, 71, 104, 113] using

---

**Figure 5.** Excluded regions (2σ) in the $M_{Z'}$-$g_{Z'}$ plane for the $B - L$ (a) and $B_\mu + L_\mu + L_\tau$ (b) models.
previous COHERENT data. Figure 5a shows the 2σ limits that we obtained from the COHERENT Ar and CsI data, compared with the limits obtained from other experiments and the \((g - 2)_\mu \) 2σ allowed band in this model. One can see that the bounds obtained by experiments using only leptonic probes are the same as those for the universal model in figure 4, because of the same magnitudes of the lepton charges (see table 1). The coupling \(g_{Z'}\) is well constrained by the accelerator experiments for large values of \(M_{Z'}\) and fixed target experiments for small values of \(M_{Z'}\). Note also that the allowed region for \((g - 2)_\mu\) is the same as that in the universal model, because the magnetic moment of the muon is not dependent on the couplings of quarks.

On the other hand, the CEνNS bounds are different from the universal model, because the \(Z'\) contribution to \(Q_{V,SM+V}\) is negative and adds to the negative SM contribution. Therefore, in figure 5a there are only the upper bounds shown by the blue-dashed, red-dashed, and black-solid lines that we obtained from the CsI, Ar, and combined analyses, respectively. These limits have the same behaviour as the corresponding ones discussed in subsection 4.1 for the universal model, but are weaker because the quark charges are smaller by a factor of 3, as shown in table 1. The numerical values of the limits for small and large values of \(M_{Z'}\) are given in table 2.

Figure 5a shows that, as in the universal model, the COHERENT CEνNS limit confirms the exclusion of the explanation of the \((g - 2)_\mu\) anomaly with the \(B - L\) model and extends the total exclusion region of non-CEνNS experiments by covering a previously not-excluded area for \(10 \text{ MeV} \lesssim M_{Z'} \lesssim 200 \text{ MeV}\) and \(5 \times 10^{-5} \lesssim g_{Z'} \lesssim 3 \times 10^{-4}\). Also in this case, the new COHERENT CEνNS limits are consistent with those obtained in ref. [26] using the first COHERENT CsI data and slightly extend the COHERENT CEνNS exclusion region.

### 4.3 \(B_y + L_\mu + L_\tau\) model

The 2σ limits that we obtained for \(g_{Z'}\) and \(M_{Z'}\) in the \(B_y + L_\mu + L_\tau\) model [113, 114] from the COHERENT Ar and CsI data are shown in figure 5b. One can see that the result of the analyses of the CsI and combined Ar and CsI data are qualitatively similar to those discussed in subsection 4.1 for the universal model: there is a lower curve that represents the upper boundary of the 2σ allowed region where the contribution of the \(Z'\) boson to \(Q_{V,SM+V}\) is small and a thin allowed strip where \(Q_{V,SM+V} \simeq -Q_{SM}\), leading to a degeneracy with the SM cross section that can fit well the data. Neglecting the form factors and the small proton SM contribution, one can find that in the case of the \(B_y + L_\mu + L_\tau\) model the thin allowed strip lies at

\[
g_{Z'}^{B_y+L_\mu+L_\tau}_{\text{strip}} \simeq \sqrt{N \over A} \sqrt{2G_F M_{Z'}^2} \simeq 3.1 \times 10^{-3} \frac{M_{Z'}}{\text{GeV}}. \tag{4.3}
\]

Under the same approximations, one can find that the cancellation between the SM and \(Z'\) contributions to \(Q_{V,SM+V}\) occurs in the parameter space between the lower upper bound curve and the thin allowed strip for

\[
g_{Z'}^{B_y+L_\mu+L_\tau}_{\text{canc}} \simeq \sqrt{N \over A} \frac{\sqrt{2G_F M_{Z'}^2}}{2} \simeq 2.2 \times 10^{-3} \frac{M_{Z'}}{\text{GeV}}. \tag{4.4}
\]
Since the Ar data are less constraining than the CsI data, the $2\sigma$ allowed region in figure 5b is that below the upper red-dashed line, with the exception of the excluded thin strip that corresponds to the cancellation condition, see eq. (4.4).

Figure 5b shows also the LHCb [150] limits on $g_{Z'}$ in the $B_y + L_\mu + L_\tau$ model and the $(g-2)_\mu$ $2\sigma$ allowed band. One can see that the LHCb bounds exclude the $(g-2)_\mu$ allowed band only for some ranges of values of $M_{Z'}$ above about 200 MeV. On the other hand, the bounds that we obtained from the analysis of the COHERENT CE$\nu$NS data exclude all the $(g-2)_\mu$ allowed band, leading to the rejection of the explanation of the $(g-2)_\mu$ anomaly with the $B_y + L_\mu + L_\tau$ model.

4.4 $B - 3L_e$ model

Figure 6a shows the $2\sigma$ limits that we obtained from the COHERENT Ar and CsI data in the $B - 3L_e$ model [102, 104, 113, 115], compared with the limits obtained from non-CE$\nu$NS experiments, which are quite strong, because there are many experiments that probe the interactions of electrons and their coupling with the $Z'$ boson in this model is three times stronger than that in the $B - L$ model. Strict limits are especially derived from $e^+e^-$ collider data.

Note that in figure 6a obviously there is no $(g-2)_e$ allowed region, because in this model the $Z'$ boson does not interact with muonic flavor. On the other hand, there is the $(g-2)_e$ obtained from the measurement of the magnetic moment of the electron [155, 156] which is compatible with the prediction at 1.6$\sigma$ level taking into account the recent determination of the fine structure constant [157].

These limits that we obtained from the combined analysis of the COHERENT CsI and Ar CE$\nu$NS data have the same behaviour as the corresponding ones for the $B - L$ model. They have also similar magnitudes, because the lack of interaction with $Z'$ of the dominant $\nu_\mu$ and $\bar{\nu}_\mu$ fluxes is compensated by the threefold increase of the $\nu_e$ coupling. The numerical values of the limits for small and large values of $M_{Z'}$ are given in table 2.

Figure 6a shows that the COHERENT CsI and Ar CE$\nu$NS data allow us to extend the total exclusion region of non-CE$\nu$NS by covering a previously not-excluded area for $10$ MeV $\lesssim M_{Z'} \lesssim 100$ MeV and $5 \times 10^{-5} \lesssim g_{Z'} \lesssim 2 \times 10^{-4}$.

4.5 $B - 3L_\mu$ model

Figure 6b shows the $2\sigma$ limits that we obtained from the COHERENT Ar and CsI data in the $B - 3L_\mu$ model [104, 113, 115], compared with the limits obtained from the LHCb [150] experiment $(Z' \rightarrow \mu^+\mu^-)$, which exist and are relatively strong only for $M_{Z'} \gtrsim 200$ MeV. The figure shows also the $(g-2)_\mu$ $2\sigma$ allowed band in this model, which is not excluded by the LHCb bounds for $M_{Z'} \lesssim 200$ MeV, but it is completely excluded by the bounds that we obtained from the analysis of the COHERENT CE$\nu$NS data.

4.6 $B - 2L_e - L_\mu$ model

In this model [104] both $\nu_e$ and $\nu_\mu$ interact with the $Z'$ boson as in the $B - L$ model, but the interaction of the subdominant $\nu_e$ flux is twice stronger. Therefore the bounds
Figure 6. Excluded regions (2$\sigma$) in the $M_{Z'}$-$g_{Z'}$ plane for the $B-3L_e$ (a) and $B-3L_\mu$ (b) models.

Figure 7. Excluded regions (2$\sigma$) in the $M_{Z'}$-$g_{Z'}$ plane for the $B-2L_e-L_\mu$ (a) and $B-L_e-2L_\mu$ (b) models.
that we obtained from the analyses of the COHERENT CEνNS data, shown in figure 7a are similar and slightly stronger than those in the $B - L$ model (see also table 2). From figure 7a one can also see that the $(g - 2)_\mu$ $2\sigma$ allowed band in this model is excluded by the total exclusion limits of non-CEνNS experiments. The analysis of the COHERENT CsI and Ar CEνNS data allows us to extend the total exclusion region of non-CEνNS experiments by covering a previously not-excluded area for $10 \text{ MeV} \lesssim M_{Z'} \lesssim 100 \text{ MeV}$ and $5 \times 10^{-5} \lesssim g_{Z'} \lesssim 2 \times 10^{-4}$.

4.7 \( B - L_e - 2L_\mu \) model

The phenomenology of this model [104] is similar to that of the $B - 2L_e - L_\mu$ model, with the difference that the bounds obtained from the COHERENT CEνNS data are stronger, because the interactions with the $Z'$ boson of the dominant $\nu_\mu$ and $\bar{\nu}_\mu$ fluxes are twice stronger than those of the subdominant $\nu_e$ flux, as one can see from figure 7a and table 2. One can also see from figure 7b that the limits from non-CEνNS are weaker than those in figure 7a for the $B - 2L_e - L_\mu$ model, whereas those obtained in $\nu_\mu$ experiments are stronger. As a result, the $(g - 2)_\mu$ $2\sigma$ allowed band in this model is not completely excluded by the results of non-CEνNS experiments, but it is completely excluded by the bounds that we obtained from the analysis of the COHERENT CsI and Ar CEνNS data. Moreover, we extend the total exclusion region of non-CEνNS experiments by covering a previously not-excluded area for $10 \text{ MeV} \lesssim M_{Z'} \lesssim 200 \text{ MeV}$ and $3 \times 10^{-5} \lesssim g_{Z'} \lesssim 3 \times 10^{-4}$.

4.8 \( L_e - L_\mu \) model

Figure 8a shows the $2\sigma$ limits that we obtained from the COHERENT Ar and CsI data in the $L_e - L_\mu$ model [76, 113, 116]. As for all the $L_\alpha - L_\beta$ models the constraints that we can obtain from CEνNS data are weaker than those in the previous models, because the interaction with quarks occurs only at loop level, and hence it is weaker. This is also shown by the values in table 2 where one can see that the bounds in the $L_\alpha - L_\beta$ are more than one order of magnitude weaker than those corresponding to the models that we considered in the previous subsections. Moreover, in spite of the fact that all the neutrino fluxes ($\nu_e$, $\nu_\mu$, and $\bar{\nu}_\mu$) interact with the $Z'$ boson in this model, the $Z'$ contribution to the CEνNS event rate is suppressed by the opposite signs of the $\nu_e$ and $\nu_\mu$ contributions to $Q_{\nu,SM+V}^V$ explained at the end of subsection 3.1 and illustrated by the red-dashed curves in figures 1c and 1d.

One can see from figure 8a that the bounds obtained from the current COHERENT CEνNS data are not competitive with those obtained from non-CEνNS experiments and do not contribute to the exclusion of the $(g - 2)_\mu$ $2\sigma$ allowed band in this model. Let us note that most of this band is excluded by non-CEνNS experiments, but there is a small non-excluded part at $M_{Z'} \approx 20 - 30 \text{ MeV}$ and $g_{Z'} \approx (4 - 7) \times 10^{-4}$.

4.9 \( L_e - L_\tau \) model

Since in the $L_e - L_\tau$ model [76, 113, 116] the dominant $\nu_\mu$ in the COHERENT experiment is not interacting with the $Z'$ boson, the bounds on the parameters of the model are rather weak. From figure 8b and table 2, one can see that they are comparable with the bounds in the $L_e - L_\mu$ model, with the difference that there is an allowed diagonal strip
for $M_{Z'} \gtrsim 50$ MeV. This occurs in the $L_e - L_\tau$ model because of the different signs of the SM and $Z'$ contributions to $Q_{V,SM+V}^V$ discussed in subsection 3.1. The allowed strip is the region of the parameters where $Q_{V,SM+V}^V \simeq -Q_{SM}^V$, leading to a degeneracy with the SM cross section, as for the similar strips in figure 4 for the universal model and figure 5b for the $B_y + L_\mu + L_\tau$ model. Neglecting the form factors and the small proton SM contribution,
this degeneracy occurs for
\[ (g_{Z^{'\ell} - \ell^\tau})_{\text{strip}} \approx \sqrt{\frac{N}{Z}} \frac{\pi G_F M_{Z'}^2}{\sqrt{2} \alpha_{EM} \varepsilon_{\tau\ell}} \approx 6 \times 10^{-2} \frac{M_{Z'}}{\text{GeV}}, \] (4.5)

where we considered \( N/Z \approx 1.3 \) and \( \varepsilon_{\tau\ell} \approx 1.5 \). One can see from figure 8b that the allowed diagonal strip lies along the line given by eq. (4.5).

The non-CEνNS bounds in figure 8b are the same as the bounds in figure 8a that have been obtained with electron-interaction experiments, including that from \((g - 2)_{\mu}\) value [155–157] that we already mentioned above in subsection 4.4 for the \( B - 3L_\ell \) model. From figure 8b one can see that in the \( L_\ell - L_\tau \) model the bounds obtained from the current COHERENT CEνNS data are not competitive with those obtained from non-CEνNS experiments and the non-CEνNS experiments exclude the CEνNS allowed diagonal strip discussed above.

4.10 \( L_\mu - L_\tau \) model

Figure 8c shows the 2σ limits that we obtained from the COHERENT Ar and CsI data in the popular \( L_\mu - L_\tau \) model [26, 28, 59, 71, 76, 78, 79, 117]. From figure 8c and the values in table 2, one can see that the bounds obtained in this model from the COHERENT CEνNS data are the strongest among the \( L_\alpha - L_\beta \) models. This is due to the interaction with the \( Z' \) boson of the dominant \( \nu_\mu \) and \( \bar{\nu}_\mu \) fluxes that is not suppressed by the opposite contribution of the \( \nu_e \) flux as in the \( L_\ell - L_\mu \) model.

From figure 8c, one can also see that there is an allowed diagonal strip that is the region of the parameters where \( Q_{V,\beta + \ell} \simeq -Q_{V,\ell} \), as discussed above for other models. Since \( \varepsilon_{\tau\mu} \approx \ln(m_{\tau}^2/m_{\mu}^2)/6 \), as discussed in subsection 3.1, the allowed diagonal strip corresponds to
\[ (g_{Z^{'\mu} - \mu^\tau})_{\text{strip}} \approx \sqrt{\frac{N}{Z}} \frac{6\pi G_F M_{Z'}^2}{2 \alpha_{EM} \ln(m_{\tau}^2/m_{\mu}^2)} \approx 7 \times 10^{-2} \frac{M_{Z'}}{\text{GeV}}, \] (4.6)

where we considered \( N/Z \approx 1.3 \)

One can see from figure 8c that in the \( L_\mu - L_\tau \) model there are several non-CEνNS constraints whose combination is more stringent than those given by the current COHERENT CEνNS data: CMS [158] \((Z \rightarrow Z'\mu\mu \rightarrow 4\mu)\), BaBar [159] \((e^+e^- \rightarrow Z'\mu\mu \rightarrow 4\mu)\), CCFR [160, 161] (neutrino trident production), and Borexino [117, 162, 163] \((Z'\)-mediated solar neutrino interactions). These non-CEνNS constraints exclude the allowed diagonal strip corresponding to eq. (4.6). On the other hand, they do not completely exclude the \((g - 2)_{\mu} \) 2σ allowed band in this model, that is shown in figure 8c. One can see that the part of this band for 10 MeV \( \lesssim M_{Z'} \lesssim 200 \) MeV and \( 3 \times 10^{-4} \lesssim g_{Z'} \lesssim 10^{-3} \) eludes the exclusions.

4.11 Scalar model

Figure 8d shows the 2σ limits that we obtained from the COHERENT Ar and CsI data in the scalar boson mediator model described in subsection 3.2. The figure shows also the \((g - 2)_{\mu} \) 2σ allowed band in this model and the constraints obtained from the measurement.
of neutrons scattering on a $^{208}$Pb target [164–166], the measurement of $\tau$, mesons, and $Z$ decays [167–172], and double-beta decay experiments [167, 173–175] (see also the summary in ref. [126]).

One can see from figure 8d that the COHERENT CE$\nu$NS constraints are much more stringent than the non-CE$\nu$NS bounds for $M_\phi \gtrsim 2$ MeV and they exclude the explanation of the $(g - 2)_\mu$ anomaly in the scalar boson mediator model.

5 Conclusions

In this paper we analyzed the recent CE$\nu$NS data obtained by the COHERENT Collaboration with the CsI and Ar detectors and we derived constraints on the coupling and mass of a non-standard light vector or scalar boson mediator considering several models that have been studied in the literature. We presented the results obtained from the separate analyses of the CsI and Ar data and those obtained from the combined analysis of the two datasets.

We considered several models with a light vector boson $Z'$: the anomalous model with universal coupling of the $Z'$ vector boson with all SM fermions (assuming that the quantum anomalies are canceled by the contributions of the non-standard fermions of an extended full theory), several anomaly-free models with gauged $U(1)'$ symmetries, as the popular $B - L$ symmetry, in which the $Z'$ vector boson couples directly to quarks and leptons, and the anomaly-free models with gauged $L_e - L_\mu$, $L_e - L_\tau$, and $L_\mu - L_\tau$ symmetries, in which the $Z'$ vector boson couples directly to the involved lepton flavors and indirectly to nucleons at the one-loop level.

We compared the constraints obtained from the COHERENT CsI and Ar CE$\nu$NS data with those obtained from several non-CE$\nu$NS experiments. We showed that the COHERENT CE$\nu$NS data allow us to extend the excluded regions of the parameters in the models in which the $Z'$ vector boson couples directly to quarks and in the universal scalar mediator model. In particular, the total excluded region is extended to smaller values of the coupling constant $g_{Z'}$ for $10$ MeV $\lesssim M_{Z'} \lesssim 100$ MeV in the universal, $B - L$, $B - 3L_e$, $B - 2L_e - L_\mu$, and $B - L_e - 2L_\mu$ models. The regions in the $M_{Z'}$-$g_{Z'}$ plane that are excluded by non-CE$\nu$NS experiments for the $B_y + L_\mu + L_\tau$ and $B - 3L_\mu$ models are limited to $M_{Z'} \gtrsim 200$ MeV. Therefore, for these models the COHERENT CE$\nu$NS data allow us to obtain a large extension of the total excluded region for $M_{Z'} \lesssim 200$ MeV.

The models in which the $Z'$ couples to muons can explain the $(g - 2)_\mu$ anomaly [29, 55, 56], and the allowed band in the $M_{Z'}$-$g_{Z'}$ plane is tested by non-CE$\nu$NS experiments, as shown in figures 4, 5, 6, and 7. The results of our analysis of the COHERENT CE$\nu$NS data exclude the explanation of the $(g - 2)_\mu$ anomaly in the models in which the $Z'$ vector boson couples directly to quarks by confirming the excluded regions of non-CE$\nu$NS experiments and extending the coverage of the $(g - 2)_\mu$ allowed band for the $B_y + L_\mu + L_\tau$, $B - 3L_\mu$, and $B - L_e - 2L_\mu$ models.

The constraints that we obtained for the $L_e - L_\mu$, $L_e - L_\tau$, and $L_\mu - L_\tau$ are less stringent because the one-loop interactions of the $Z'$ vector boson with the nucleons is weaker than the direct interaction. For these models the current COHERENT CE$\nu$NS data allow us to
confirm the exclusion of part of the parameter space that is already covered by non-CEνNS experiments, but cannot probe the \((g - 2)_{\mu}\) allowed band in the \(L_e - L_\mu\) and \(L_\mu - L_\tau\) models.

We finally considered CEνNS interactions mediated by a light scalar boson \(\phi\) assuming for simplicity a universal coupling with the quarks and neutrinos involved in the CEνNS processes measured in the COHERENT experiment. We obtained the strong constraints on the mass \(M_\phi\) and coupling of the scalar boson shown in figure 8d that greatly extend the region excluded by non-CEνNS experiments and rejects the explanation of the \((g - 2)_{\mu}\) anomaly in this model.

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A \(Z'\) coupling

There is some confusion on the value of the coefficient of the contribution of a new \(Z'\) vector boson mediator in eq. (3.7) that is obtained assuming the interaction Lagrangian in eq. (3.6). For example, in refs. [6, 12, 15, 16, 99, 100] the coefficient is half of that in eq. (3.7). On the other hand, the coefficient in refs. [14, 19, 25, 26, 70, 71, 101–105] agrees with that in eq. (3.7). In this appendix we prove that the coefficient in eq. (3.7) is the right one.
Let us start by considering the relevant vector part of the Standard Model neutral-current weak interaction Lagrangian (see, e.g., refs. [85, 110])

\[
L^V_Z = -\frac{g}{2\cos\theta_W} Z_\mu \left[ 2 g^V_\nu \sum_{\ell=e,\mu,\tau} \bar{\nu}_\ell \gamma^\mu \nu_\ell L + \sum_{q=u,d} g^q_V \bar{q} \gamma^\mu q \right],
\]

(A.1)

with the tree-level couplings

\[
g^V_\nu = \frac{1}{2}, \quad g^V_q = \frac{1}{2} - \frac{4}{3} \sin^2\theta_W, \quad \text{and} \quad g^d_V = -\frac{1}{2} + \frac{2}{3} \sin^2\theta_W.
\]

(A.2)

Confronting eq. (A.1) with the Lagrangian (3.6), one can see that the \(Z'\) vector interaction of left-handed neutrinos with quarks is obtained from the vector part of the Standard Model neutral-current interaction with the substitutions

\[
\frac{g}{2\cos\theta_W} 2g^V_\nu \rightarrow g^{\nu V}_Z, \quad \frac{g}{2\cos\theta_W} g^q_V \rightarrow g^q_{Z' V}, \quad \text{and} \quad m_Z \rightarrow m_{Z'}.
\]

(A.3)

This correspondence is shown in figure 9, where we depicted the two Feynman diagrams that describe the neutrino-quarks interactions that contribute to CE\(\nu\)NS at tree level. The total amplitude is given by the sum of the two diagrams

\[
A \propto \frac{g^2}{4\cos^2\theta_W} \frac{2g^V_\nu g^q_V}{q^2 - m^2_Z} + \frac{g^{\nu V}_Z g^q_{Z'} V}{q^2 - m^2_{Z'}}.
\]

(A.4)

Taking into account that \(g^\nu_V = 1/2\) and

\[
\frac{g^2}{4\cos^2\theta_W m^2_Z} = \sqrt{2} G_F,
\]

(A.5)

for \(q^2 \ll m^2_Z\) we obtain

\[
A \propto g^\nu_V + \frac{g^{\nu V}_Z g^q_{Z'}}{\sqrt{2} G_F (q^2 - m^2_{Z'})}.
\]

(A.6)

This relation leads to eq. (3.7), taking into account that the conservation of the vector current implies that

\[
g^{\nu V}_{Z'} = 2g^{\nu V}_Z + g^{dV}_{Z'} \quad \text{and} \quad g^{n V}_{Z'} = g^{n V}_Z + 2g^{dV}_{Z'}.
\]

(A.7)

In conclusion of this appendix, let us note that the results of the analyses in refs. [6, 12, 15, 16, 99, 100], where the \(Z'\) contribution to the weak charge in CE\(\nu\)NS is half of that in eq. (3.7), must be reinterpreted by rescaling their \(Z'\) coupling \(g_{Z'}\) by a factor \(\sqrt{2}\).

B Muon \(g - 2\)

Recently, the Fermilab Muon \(g - 2\) experiment [56] confirmed the value of the muon anomalous magnetic moment \((g - 2)_\mu\) that was measured in 2006 in the Muon E821 experiment at Brookhaven National Laboratory [55], leading to the combined 4.2\(\sigma\) deviation from the Standard Model prediction

\[
\Delta a_\mu = (25.1 \pm 5.9) \times 10^{-10},
\]

(B.1)
where $a_\mu = (g - 2)_\mu/2$. This $(g - 2)_\mu$ anomaly may be due to new physics beyond the SM (see the reviews in refs. [68, 176, 177]).

In theories beyond the SM, an additional neutral boson $B$ with mass $M_B$, which interacts with muons with coupling $g_B$, contributes to the muon anomalous magnetic moment with [178]

$$
\delta a_\mu^B = \frac{g_B^2}{8\pi^2} \frac{Q(x)}{x^2 + (1 - x) M_B^2/m_\mu^2}
$$

where $Q(x)$ depends on the scalar or vector nature of the neutral boson $B$:

$$
Q(x) = \begin{cases} 
  x^2 (2 - x) & \text{(scalar)}, \\
  2x^2 (1 - x) & \text{(vector)}. 
\end{cases}
$$

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