Let us look at a special type of context sensitive grammars, the so-called Definite Clause Grammars, or DCG, as described by Pereira and Warren (1980).

The following question seems natural here:

- Can every context sensitive language be described by means of a definite clause grammar?

The question must be answered in the affirmative, as can be seen by simulating Turing machines or better Markov algorithms by means of definite clause grammars. This means that the definite clause grammars have at least the same computational power as the grammars of Chomsky type 0. And hence theoretically speaking they can also handle languages of Chomsky type 1.

If we focus on the question which practical methods have been developed to handle context sensitive languages by means of definite clause grammars or similar formalisms then the situation is much more unclear. It seems to be a problem with a considerable actual research effort. We may see the occurring of several new grammar types as the results of exactly this tendency, for instance Gapping Grammars in (Dahl & Abramson 1984, Dahl 1984) and Puzzle Grammars (Sabatier 1984).

The next natural and fundamental question seems to be the following:

- Does there exist any known problems within the languages that can be described by means of definite clause grammars?

It should be answered in the affirmative, actually there exist many problems. As an example we may look at possibly the most famous problem, the coordination problem.

The text that we want to examine consists simply of the Danish sentence

- Peter ønsker ikke at spise et æble.

(Peter does not want to eat an apple)

What should be the output or the result of the process corresponding to this sentence as input? It should be a sort of semantic representation providing a reasonable picture of the meaning of the statement. We tend to argue for the use of logical representations, and also here in the choice of semantic representation, so the notion logico-semantic representation seems to be justified.

Are we able to construct an automatic translation of an appropriate sublanguage into such a logico-semantic representation? Yes, for example it can be done by a Prolog program like the one described in the appendix. (Presumably we wanted a DCG describing the same translation, but in the used version of Micro-Prolog there is no support of DCGs).

During such an execution the result variable obtains a value to be output like this:

\[
\text{(Not} \ (\text{Oensker} \ Peter \ (\text{Exist} \ x \ ((x \ (\text{Is} \ \text{Aeble}) \ And \ (\text{Spise} \ Peter \ x))))))
\]
which corresponds to the following logical formula in a more traditional notation:

\[ \neg \text{ønsker}(Peter, \exists x (\text{Æble}(x) \land \text{Spiser}(Peter, x))) \,.
\]

We notice that this seems to be a so-called intensional reading, and that Montague grammars here show themselves (Montague 1974). Perhaps we rather wanted a so-called extensional reading like the following formula:

\[ \forall x (\text{Æble}(x) \rightarrow \neg \text{ønsker}(Peter, \text{Spiser}(Peter, x))) \,.
\]

The problem here seems to be due to scope problems, and this is exactly the wanted example of the coordination problem.

Another reasonable question is: what do the simplest logico-semantic assignments (or representation transformations) look like? That question seems to have a trivial answer, namely the constant assignment functions mapping everything into e.g. false. So we should probably modify the question a little:

- How can we characterize the simplest non-constant logico-semantic assignments?

To give a reasonable answer to this question we should discuss further what does the term "simplest" mean in this context.

Let us suppose that simplicity involves Frege's principle for referential transparency.

Under the assumption of the principle of referential transparency we can argue that a particular assignment is the simplest possible one, viz. an assignment giving a mixture of lambda calculus expressions and predicate calculus expressions as the logico-semantic representation.

It seems justified to call this representation a denotational semantic representation, in the style of (Milne & Strachey 1976, Gordon 1979).

Before presenting this denotational semantic assignment function called Sem, it seems appropriate to look at yet another little grammar G2 and its treatment by means of definite clause grammars. (Figure 3)

Perhaps we ought to show the system's treatment of a few selected sentences. The sentences are the following:

- En mand spiser et æble med skræl
  (a man eats an apple with the peel)

- Enhver ung mand elsker en smuk kvinde.
  (every young man loves a beatiful woman)

See the figures 1 and 2.
en mand spiser et æble med skræl

\[ S(z) \]

\[ NP(x \ y \ z) \]

\[ VP(x \ y) \]

\[ Det(x \ w \ y \ z) \]

\[ NP2(x \ w) \]

\[ \exists x[w \& y] \]

\[ Noun(x \ w) \]

\[ Is(x, Mand) \]

\[ Tverb(x \ w1 \ z1) \]

\[ NP(w1 \ z1 \ y) \]

\[ Spiser(x, w1) \]

\[ Det(w1 \ w2 \ z1 \ y) \]

\[ NP2(w1 \ w2) \]

\[ y1 \& w3 \]

\[ \exists w1[w2\& z1] \]

\[ NP2(w1 \ y1)PP(z2 \ w1 \ w3) \]

\[ Noun(w1 \ y1) \]

\[ Is(w1, Æble) \]

\[ Prep(z2) \]

\[ NP(x1) \ w3) \]

\[ Mod \]

\[ z2(w1, x1) \& w4 \]

\[ NP2(x1 \ w4) \]

\[ Noun(x1 \ w4) \]

\[ Is(x1, Skræl) \]

en. mand spiser et æble med skræl
dvs.

\[ z = \exists x[w \& y] \]

\[ = \exists x[w \& \exists w1[w2\& z1]] \]

\[ = \exists x[w \& \exists w1[y1 \& w3 \& z1]] \]

\[ = \exists x[Is(x, Mand) \& \exists w1[Is(w1, Æble) \& w3 \& Spiser(x, w1)]] \]

\[ = \exists x[Is(x, Mand) \& \exists w1[Is(w1, Æble) \& z2(w1, x1) \& w4 \& Spiser(x, w1)]] \]

\[ = \exists x[Is(x, Mand) \& \exists w1[Is(w1, Æble) \& Med(w1, x1) \& Is(x1, Skræl) \& Spiser(x, w1)]] \]

\[ Figure 1 \]
enhver ung mand elsker en smuk kvinde

\[ z = \forall x [w \rightarrow y] \]
\[ = \forall x [w_1 \& y_1 \rightarrow y] \]
\[ = \forall x [w_1 \& y_1 \rightarrow \exists w_2 [w_3 \& z_1]] \]
\[ = \forall x [w_1 \& y_1 \rightarrow \exists w_2 [w_4 \& y_2 \& z_1]] \]
\[ = \forall x [\text{Is}(x, Ung) \& \text{Is}(x, Mand) \rightarrow \exists w_2 [\text{Is}(w_2, Smuk) \& \text{Is}(w_2, Kvinde) \& \text{Elsker}(x, w_2)]] \]
\[ = \forall x [\text{Is}(x, Ung) \& \text{Is}(x, Mand) \rightarrow \exists \text{Is}(y, Smuk) \& \text{Is}(y, Kvinde) \& \text{Elsker}(x, y)] \]

**Figure 2**
Now let us return to the problem to construct the simplest possible logico-semantic assignment function. We can make two assertions here:

**Assertion A:**
The following logico-semantic assignment function $Sem$ in the grammar $G2$ is the simplest non-constant assignment function according to the mentioned criteria.

**Assertion B:**
The logico-semantic representation of a text by means of this denotational semantic assignment function $Sem$ is identical to the corresponding logico-semantic representation of the text in the grammar $G2$ (which is the output corresponding to the result variable $z$ when executing the definite clause grammar corresponding to $G2$).

The assertion A may be demonstrated to hold by always choosing the simplest possible alternatives.

The assertion B may be proven formally (though not possible within the limits of this paper), but the assertion may also be accepted by looking at a few examples. Let us try, using the example grammar $G2$ and the small texts above.

```
S → NP VP
NP → Det NP2
NP → NP2
NP2 → Noun
NP2 → Adj NP2
NP2 → NP2 PP
PP → Prep NP
VP → IVerb
NP → TVerb NP
VP → VP PP
Det → enhver
Det → ethvert
Det → en
Det → et
Det → hvilken
Det → hvilket
```

*Figure 3*
Sem("en mand spiser et æble med skræl")
= Sem(en^mand^spiser^et^æble^med^skræl)
= Sem(D1^N1^Tv^D2^N2^P^Nart)
= Combine[D,N,Tv,D,N,P,Nart]{Sem(D1),Sem(N1)Sem(Tv),Sem(D2),Sem(N2),Sem(P),Sem(Nart))
= Sem(D1)(Sem(N1),\lambda t. [Sem(D2) (Sem(N2) & (Sem(P) o Sem(Nart))),
First(Sem(Tv),t)])
= Sem(D1)(Sem(N1),\lambda t. [Sem(D2) (Sem(N2) & (Sem(P) o Sem(Nart))),
First(\lambda (u,v).Tv(u,v),t)])
= Sem(D1)(Sem(N1),\lambda t. [Sem(D2) (Sem(N2) & (Sem(P) o Sem(Nart))),
\lambda v.Tv(t,v)])
= Sem(D1)(Sem(N1),\lambda t. [(\lambda (u,w).3y[u(y) & w(y)])
(\lambda v.Is(v,N2) & (\lambda (s,t).P(s,t) o Nart)),\lambda v.Tv(t,v))]
= Sem(D1)(Sem(N1),\lambda t. [(\lambda (u,w).3y[u(y) & w(y)])
(\lambda v.Is(v,N2) & (\lambda s.P(s,Nart)),\lambda v.Tv(t,v))]
= Sem(D1)(Sem(N1),\lambda t. [(\lambda (u,w).3y[u(y) & w(y)])
(\lambda s.Is(s,N2) & P(s,Nart)),\lambda v.Tv(t,v))]
= Sem(D1)(Sem(N1),\lambda t.3y[(\lambda s.Is(s,N1))(x) & (\lambda v.Is(y,N2) & P(y,Nart) & Tv(t,y))(y)]
= \exists x[(\lambda s.Is(s,N1))(x) & (\lambda v.Is(y,N2) & P(y,Nart) & Tv(t,y))(x)]
Sem("enhver ung mand elsker en smuk kvinde")
= Sem(enhver^ung^mand^elsker^en^smuk^kvinde)
= Sem(D1^N1^Tv^D2^A2^N2)
= Combine[D,A,N,Tv,D,A,N]{Sem(D1),Sem(A1),Sem(N1),Sem(Tv),Sem(D2),Sem(A2),Sem(N2))
= Sem(D1) (Sem(A1) && Sem(N1),
  λt.(Sem(D2)(Sem(A2) && Sem(N2), First(Sem(Tv),t))))
= Sem(D1) (Sem(A1) && Sem(N1),
  λt.(Sem(D2)(λu.Is(u,A2) && λv.Is(v,N2),
    First(λ(x,y).Tv(x,y),t))))
= Sem(D1) (Sem(A1) && Sem(N1),
  λt.(Sem(D2)(λu.(Is(u,A2) & Is(u,N2)),λy.Tv(t,y))))
= Sem(D1) (Sem(A1) && Sem(N1),
  λt.((λ(x,z).∃v[x(v)&z(v)])(λu.(Is(u,A2) & Is(u,N2)),
    λy.Tv(t,y))))
= Sem(D1) (Sem(A1) && Sem(N1),
  λt.(∃v[(λu.(Is(u,A2) & Is(u,N2))(v)&(λy.Tv(t,y))(v))])
  = (λ(y,z).∀x[y(x)⇒z(x)])(λu.Is(u,A1))(&(λv.Is(v,N1))),
  λt.(∃v[Is(v,A2)&Is(v,N2)&Tv(t,v)]))
= (λ(y,z).∀x[y(x)⇒z(x)])(λu.Is(u,A1) & Is(u,N1)),
  λt.(∃v[Is(v,A2) & Is(v,N2) & Tv(t,v)]))
= ∀x[(λu.(Is(u,A1) & Is(u,N1))(x)
  ⇒(λt.(∃v[Is(v,A2) & Is(v,N2) & Tv(t,v)])(x)))]
= ∀x[Is(x,A1) & Is(x,N1)⇒∃v[Is(v,A2) & Is(v,N2) & Tv(x,v)]]
= ∀x[Is(x,Ung) & Is(x,Mand)
  ⇒∃v[Is(v,Smuk) & Is(v,Kvinde) & Elsker(x,v)]]
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Appendix

\textbf{Dt} (X Y Z) if
\textbf{Ds} (X Y Z)

\textbf{Dt} (((Which X (Y And Z)) x y) if
  \textbf{c} (hvilken x z) and
  \textbf{Dn} (X Y z X1) and
  \textbf{Dvp} (X Z X1 y)

\textbf{Dt} (((Which X (Y And Z)) x y) if
  \textbf{c} (hvilket x z) and
  \textbf{Dn} (X Y z X1) and
  \textbf{Dvp} (X Z X1 y)

\textbf{Ds1} (X Y Z) if
  \textbf{Dnp} (x y X Y z) and
  \textbf{Dvp} (x y z Z)

\textbf{Ds} (((X And Y) Z x) if
  \textbf{Ds1} (X Z y) and
  \textbf{c} (og y z) and
  \textbf{Ds} (Y z x)

\textbf{Ds} (X Y Z) if
  \textbf{Ds1} (X Y Z)

\textbf{Ds} (((X Imp Y) Z x) if
  \textbf{c} (hvis Z y) and
  \textbf{Ds} (X y z) and
  \textbf{c} (saa z X1) and
  \textbf{c} (gaelder X1 Y1) and
  \textbf{c} (at Y1 Z1) and
  \textbf{Ds} (Y Z1 x)

\textbf{Dnp} (X Y Z x y) if
  \textbf{Dprop} (X Z x)

\textbf{Drc} (X Y Z Z)

\textbf{Drc} (X Y (Y And Z) x y) if
  \textbf{c} (der x z) and
  \textbf{Dvp} (X Z z y)

\textbf{Drc} (X Y (Y And (Not Z)) x y) if
  \textbf{c} (der x z) and
  \textbf{c} (ikke z X1) and
  \textbf{Dvp} (X Z X1 y)

\textbf{Drc} (X Y (Y And (Not Z)) x y) if
  \textbf{c} (som x z) and
  \textbf{Dnp} (X1 Y1 Z z Z1) and
  \textbf{Dtv} (X1 X Y1 Z1 y)

\textbf{Drc} (X Y (Y And (Not Z)) x y) if
  \textbf{c} (som x z) and
  \textbf{Dnp} (X1 Y1 Z z Z1) and
  \textbf{Dtv} (X1 X Y1 x1 y)

\textbf{Dvp1} (X (Not Y) Z x) if
  \textbf{Dnegvp} (X Y Z x)

\textbf{Dvp1} (X Y Z x) if
  \textbf{Ddovp} (X Y Z x)
Dvp (X \( Y \And Z \)) \( x \ y \) if
Dvp1 (X \( Y \ x \ z \)) and
\( \text{c (og z X1)} \) and
Dvp (X \( Z \ X1 \) \( y \))

Dvp (X \( Y \ Z \) \( x \)) if
\( \text{Dvp1 (X \( Y \ Z \) \( x \))} \)

Dnegvp (X \( Y \ Z \) \( x \)) if
\( \text{Dvp-vp (X y \( Y \ Z \) z) and} \)
\( \text{c (ikke z X1)} \) and
\( \text{c (at X1 Y1)} \) and
Di (X \( y \ Y1 \) \( x \))

Dnegvp (X \( Y \ Z \) \( x \)) if
\( \text{Dtv (X y \( Y \ Z \) X1) and} \)
\( \text{c (ikke X1 Y1)} \) and
Dvp (y \( z \ Y1 \) \( X1 \) \( x \))

Dnegvp (X \( Y \ Z \) \( x \)) if
\( \text{Div (X \( Y \ Z \) y) and} \)
\( \text{c (ikke y X x)} \)

\( \text{Dposvp (X \( Y \ Z \) \( x \)) if} \)
\( \text{Dvp-vp (X y \( Y \ Z \) z) and} \)
\( \text{c (at z X1)} \) and
Di (X \( y \ X1 \) \( x \))

Dposvp (X \( Y \ Z \) \( x \)) if
\( \text{Dtv (X y \( y \ Z \) z X1) and} \)
\( \text{Dvp (y \( z \ Y \) X1 \( x \))} \)

Dposvp (X \( Y \ Z \) \( x \)) if
\( \text{Div (X \( Y \ Z \) x) if} \)
\( \text{Di (X \( Y \ Z \) x) if} \)
\( \text{Di (X \( Y \ Z \) \( x \)) if} \)
\( \text{Di (X \( Y \ Z \) \( x \)) if} \)

\( \text{Dvp-vp (X y \( Y \ Z \) z) and} \)
\( \text{c (at z X1)} \) and
Di (X \( y \ X1 \) \( x \))

Dd (X \( Y \ Z \) (All X (Y Imp Z))) \( x \ y \) if
\( \text{c (enhver x y)} \)

Dd (X \( Y \ Z \) (All X (Y Imp Z))) \( x \ y \) if
\( \text{c (ethvert x y)} \)

Dd (X \( Y \ Z \) (Exist X (Y And Z))) \( x \ y \) if
\( \text{c (en x y)} \)

Dd (X \( Y \ Z \) (Exist X (Y And Z))) \( x \ y \) if
\( \text{c (let x y)} \)

\( \text{Div (X (Y X) Z x) if} \)
\( \text{c (Y Z x) and} \)
\( \text{Diverbs (y) and} \)
\( \text{Y Member y} \)

Dtv (X \( Y \) (Z X Y) \( x \ y \) if
\( \text{c (Z x y) and} \)
\( \text{Dtv (Z y) (z) and} \)
\( \text{Z Member z} \)
Dvp-vp (X Y (Z X Y) x y) if
  c (Z x y) and
  Dvp-vps (z) and
  Z Member z

Dii (X (Y X) Z x) if
  c (Y Z x) and
  Diinfs (y) and
  Y Member y

Dti (X Y (Z X Y) x y) if
  c (Z x y) and
  Dtinfs (z) and
  Z Member z

Dvp-vpi (X Y (Z X Y) x y) if
  c (Z x y) and
  Dvp-vpinfs (z) and
  Z Member z

Dn (X (X Is Y) Z x) if
  c (Y Z x) and
  Dnouns (y) and
  Y Member y

Dprop (X Y Z) if
  c (X Y Z) and
  Dprops (x) and
  X Member x

Diverbs ((lever blomstrer smiler flyver))
Dtverbs ((elsker spiser er har holder-af bestiger))
Dvp-vps ((oensker haaber))
Diinfs ((leve blomstre smile flyve))
Dtinfs ((elske spise vaere have holde-af bestige))
Dvp-vpinfs ((oenske haabe))
Dnouns ((kvinde æble mand soft-ice fugl træ medlem skisportsmand... menneske ting))
Dprops ((Mary John Peter Prolog Tony Mike sne regn))