Joint Optimization of Autonomous Electric Vehicle Fleet Operations and Charging Station Siting

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Abstract—Charging infrastructure is the coupling link between power and transportation networks, thus determining charging station siting is necessary for planning of power and transportation systems. While previous works have either optimized for charging station siting given historic travel behavior, or optimized fleet routing and charging given an assumed placement of the stations, this paper introduces a linear program that optimizes for station siting and macroscopic fleet operations in a joint fashion. Given an electricity retail rate and a set of travel demand requests, the optimization minimizes total cost for an autonomous EV fleet comprising of travel costs, station procurement costs, fleet procurement costs, and electricity costs, including demand charges. Specifically, the optimization returns the number of charging plugs for each charging rate (e.g., Level 2, DC fast charging) at each candidate location, as well as the optimal routing and charging of the fleet. From a case-study of an electric vehicle fleet operating in San Francisco, our results show that, albeit with range limitations, small EVs with low procurement costs and high energy efficiencies are the most cost-effective in terms of total ownership costs. Furthermore, the optimal siting of charging stations is more spatially distributed than the current siting of stations, consisting mainly of high-power Level 2 AC stations (16.8 kW) with a small share of DC fast charging stations and no standard 7.7kW Level 2 stations. Optimal siting reduces the total costs, empty vehicle travel, and peak charging load by up to 10%.

I. INTRODUCTION

Electrification and vehicle autonomy are driving down the total cost of ownership for vehicle fleets. Presently, autonomous electric vehicles (EVs) are being developed for fleet applications such as passenger mobility-on-demand services. The development of these Electric Autonomous Mobility-on-Demand (E-AMoD) fleets are motivated by the low maintenance and energy costs of EVs [1], low operating costs of shared autonomous vehicles [2], and policy mandates for the decarbonization of the transportation sector [3]. Autonomous fleets also have the advantage of highly controllable routing and charge scheduling compared to privately owned human-operated EVs. However, in all these developments, the optimal planning for the charging infrastructure needed to support future mobility fleets at scale is not well understood, considering the intersection of emerging trends in mobility-on-demand services, vehicle electrification, and driving automation. Crucially, the operation of future E-AMoD systems will be strongly influenced by the available charging infrastructure, which in turn should be designed to accommodate the EVs’ charging activities in the best possible way. These problems are intimately coupled, calling for optimization methods to systematically solve them. Against this background, this paper proposes a convex optimization framework to jointly optimize the design of the charging infrastructure and the operation of a centrally controlled E-AMoD fleet.

a) Literature review: This paper contributes to two main research streams. The first stream focuses on the routing and charge scheduling problem of fleet EVs. Network flow models have been successfully used to minimize fleet travel and electricity costs subject to fulfillment of customer trip requests, limited driving range, and charging constraints imposed by congestion on the power transmission grid [4], also accounting for the distribution grid [5]. A vehicle coordination and charge scheduling algorithm is proposed in [6] to efficiently optimize the operation of an E-AMoD fleet accounting for the battery level of individual vehicles and the energy availability in the power grid. A heuristic algorithm for the electric traveling salesman with time windows is developed in [7] to solve customer routing and recharging in small-scale problems. However, the optimized operations are determined for an assumed siting layout of charging stations. The second stream focuses on the design of the charging infrastructure considering the EVs’ operations as exogenous data. Previous works have largely framed the station siting problem as solving variants of mixed integer linear programs [8]–[10]. Thereby, the objective terms commonly include user access costs and station construction costs under assumptions of desired user charging behavior, determined from historic origin-destination travel data or parking dwell times. However, this class of models do not consider the greater charging flexibility of autonomous fleet vehicles, due to their capability to operate after user drop-off and reposition to alternate charging locations. Furthermore, these combinatorial optimization approaches suffer from computational scalability as their complexity rises significantly with the problem size. In conclusion, while the former research stream focuses on optimizing the E-AMoD activities for a given charging infrastructure, the latter stream bases the infrastructure design problem on historic travel data and frames it as a mixed-integer problem.
b) Statement of contribution: This paper bridges the gap between the aforementioned research streams and, rather than considering separate optimization problems, efficiently solves for the station planning and macroscopic fleet operations jointly. Specifically, we first propose a network flow model describing the EVs’ routing and charging activities and combine it with the design of the fleet size and the infrastructure siting. Second, we frame the optimal design and control problem minimizing the total cost incurred by the E-AMoD operator (defined as the sum of the fleet’s routing and charging costs, and the procurement costs for the fleet and infrastructure design) as a linear program that can be efficiently solved with off-the-shelf optimization algorithms. Finally, we showcase our framework on a case study for San Francisco, CA, where we investigate the impact of the EV type on the resulting optimal design and operation, and highlight the importance of jointly optimizing the E-AMoD system’s routing and charging with the infrastructure siting.

c) Organization: The remainder of the paper is structured as follows: Section II introduces the E-AMoD charging station siting joint optimization model. Section III details our case study of San Francisco, CA, and presents results on how the joint optimization varies with EV models of differing battery sizes, and how the joint optimization performs when compared to a baseline based upon present-day charging stations. We conclude the paper in Section IV with a summary of our key findings and an outlook for future research.

II. MODELING THE JOINT OPTIMIZATION OF E-AMoD SYSTEMS AND CHARGING STATION SITING

An E-AMoD system consists of electric autonomous fleet vehicles that serve customer travel requests. When vehicles are not serving customers, they may be recharging or performing rebalancing trips. Recharging can vary spatially, temporally, and also by charging rate. Rebalancing trips, defined as vehicle travel without carrying a customer, serve to reposition vehicles to charging stations in advance of charging events, or to resolve spatial and temporal mismatches between the origins and destinations of customer travel requests.

In previous works, the E-AMoD system is modeled as a network flow problem, utilizing an expanded road graph that has vertices representing coordinates in location, time, and battery charge level [4],[5]. In this section, we will present a new E-AMoD model that extends from the original model by introducing electricity demand charges, charge throttling, and the joint optimization of charging station siting. We will sequentially detail each component of model before presenting the complete E-AMoD problem at the end of the section.

a) Expanded graph representation: We model a transportation network as a directed graph \( G = (V_R, A_R) \) with a set of vertices \( v \in V_R \) representing locations and a set of arcs \( (v, w) \in A_R \) representing the route between \( v \) and \( w \). Each arc \((v, w)\in A_R\) is characterized by the route’s distance \( d_{v,w} \), travel time \( t_{v,w} \), and energy required to traverse it \( c_{v,w} \). In contrast with [4] and [5], we allow for self-loop arcs to capture travel demand that begins and ends in the same location, as the locations can represent city regions.

We define \( T = \{1, \ldots, T\} \) as the set of equidistant time steps of duration \( \Delta t \in \mathbb{R}^+ \), and \( C = \{1, \ldots, C\} \) as the set of equidistant battery charge level discretizations, each with energy \( E_c \in \mathbb{R}^+ \). The battery charge levels indicate the state-of-charge (SoC) levels of an EV, with \( c = 1 \) representing an empty battery and \( c = C \) representing a full battery.

The locations in \( V_R \) represent destinations for customer travel and also points of access to charging stations. We define \( S \) as the set of charging stations in the network, with each station \( s \in S \) defined by a tuple \( s = (v_s, \delta_s) \) where \( v_s \in V_R \) is the station’s location and \( \delta_s \in \mathbb{R}^+ \) is the station’s per-plug charging rate. Additionally, each station \( s \in S \) has a number of plugs, \( S_s \in \mathbb{R}^+ \). Note that in contrast with [4] and [5], this model allows for multiple stations with different charging rates to be situated at the same location.

We then define the directed multigraph \( G = (V, A) \) as the expanded transportation network, which expands \( G_R \) along the dimensions of time and battery charge level. The vertex set \( V \subseteq V_R \times T \times C \) contains vertices \( v \in V \) that are defined by the tuple \((v, t, SoC)\) in which entries specify location, time, and SoC, respectively.

The arc set \( A \) is the union of two disjoint subsets, \( A_T \cup A_S \). Travel in the transportation network is represented by arcs \((v, w) \in A_T \) and is defined by

\[
A_T = \{ (v, w) \in A \mid (v, v) \in A_R, t_w - t_v = t_{v,v}, c_v - c_w = c_{v,v} \}.
\]

This definition enforces that the time expansion for travel from \( v \) to \( w \) is equal to the travel time \( t_{v,v} \) and charge expansion is equal to the travel charge \( c_{v,v} \). Unlike in \( G_R \), the distance, travel time, and travel energy between two locations in \( G \) can be time-varying. Idling vehicles, which only move forward in time from \( v \) to \( w \) but remain fixed in location and SoC, are a subset of \( A_T \):

\[
A_I = \{ (v, w) \in A_T \mid v = v, t_w = t_v + 1, c_v = c_w \}.
\]

Recharging at charging stations is represented by arcs \((v, w) \in A_S \) and is defined by

\[
A_S = \{ (v, w) \in A \mid v = v, t_w = t_v, (c_v - c_w)E_c = \delta, \delta \in \{ \frac{E_c}{\Delta t}, \frac{2E_c}{\Delta t}, \ldots, \delta_s \} \}.
\]

This definition enforces that for the recharging process represented by the arc \((v, w)\), the location is fixed to the location of a station \( s \), the recharging occurs over one time step, and the charge rate derived from the arc’s charge expansion is at most the charge rating of the station. In contrast with [4] and [5], we allow for charging at station \( s \) to include rates below its rated capacity in order to model charge throttling, a feature that is becoming increasingly common in modern
charging stations and EVs that allows for greater control over power demand [11]. Note that at locations with multiple charging stations, multiple edges will be defined for a given pair \((v, w)\), thereby making \(G\) a multigraph.

b) Customer travel requests: We define \(\mathcal{M} = \{1, ..., M\}\) as the set of travel requests which the E-AMoD fleet must serve. Each request \(m \in \mathcal{M}\) is defined by a tuple \(m = (v_m, w_m, t_m, \lambda_m) \in V_R \times V_R \times T \times R^+\) in which the entries represent the origin, destination, departure time, and travel demand volume, respectively. We define
\[
\mathbb{1}(v, w, m) = \mathbb{1}(v_m, w_m, t_m) = (v_m, w_m, t_m) - (v, w, t) = (v_m, w_m, t_m) - (v, w, t)
\]
as an indicator for whether arc \((v, w) \in \mathcal{A}\) fulfills request \(m\). The distance, travel time, and travel energy of each arc \((v, w) \in \mathcal{A}_T\) is consistent with the distance, travel time, and travel energy of the travel request \(m\) which the arc fulfills.

c) Vehicle flows: In the E-AMoD network flow problem, we solve for vehicle flows on the expanded graph \(G\). We define \(f(v, w) : \mathcal{A} \to R^+\) to represent vehicle flow on arc \((v, w)\). The distance of the vehicles depends upon the arc \((v, w)\). If \((v, w) \in \mathcal{A}_T\), then vehicles are idling. If \((v, w) \in \mathcal{A}_S\), then the vehicles are recharging. If \((v, w) \in \mathcal{A}_T-\mathcal{A}_T\), then vehicles could be carrying customers or rebalancing. In the E-AMoD problem presented in this paper, the fleet must serve all customer travel requests as a hard constraint. Therefore, any travel along \((v, w) \in \mathcal{A}_T\) in excess of the customer travel demand must be rebalancing flow. We define \(f_0(v, w) : \mathcal{A} \to R^+\) to represent vehicle rebalance flow on arc \((v, w)\). Note that \(f_0(v, w) \leq f(v, w)\) \(\forall (v, w) \in \mathcal{A}\) as rebalancing flow on a given arc must be a fraction of the total flow of that arc. Once \(f\) is determined, the rebalancing flow \(f_0\) can be recovered post-optimization. For every \((v, w) \in \mathcal{A}_T\) and \(m \in \mathcal{M}\), if \(\mathbb{1}(v, w, m) = 1\), we compute
\[
f_0(v, w) = \max\{\sum_{(v', w') \in \mathcal{A}_T-\mathcal{A}_T: \mathbb{1}(v', w', m) = 1} (c_w - c_v)E_c \Delta t \}
\]
Here, we assume rebalancing travel is distributed uniformly among the arcs satisfying \(\mathbb{1}(v, w, m) = 1\). For any arcs \((v, w) \in \mathcal{A}_T\) that do not correspond to any travel request, \(f_0(v, w) = f(v, w)\).

d) Electricity demand charges: To introduce the modeling of electricity demand charges incurred by the fleet for their peak charging load at each location, we define \(P_{\text{max}}\).
\[
P_{\text{max}}(v) = \max_{t \in T} \sum_{(v, w) \in \mathcal{A}_S} \mathbb{1}(v, w, t) f(v, w) \frac{(c_w - c_v)E_c}{\Delta t} \quad \forall v \in V_R
\]
Here, we compute the total charging demand at location \(v\) and time \(t\) by including all associated charging arcs and taking the sum product of vehicle flow of the arc and the arc’s charge expansion, with appropriate conversions for units of power. We then take the maximum over all times to determine \(P_{\text{max}}\).

e) Charging station siting: To introduce optimal sizing of stations of varying charging rate and location, we make the number of plugs \(S_{\text{r}}\) at each station \(s \in \mathcal{S}\) an optimization variable in the E-AMoD problem. Because our model allows for charge throttling, the determination of number of plugs for slower charging rate stations is dependent upon the residual capacity of any co-located faster rate stations. To assist with the derivation of the equations that determine charging station sizing, we use an example.

First, we define \(D_v\) as the ordered set (least to greatest) of charging rates at location \(v \in V_R\). Let \(D_v(j)\) return the \(j^{th}\) element of \(D_v\) for all \(j \in \{1, ..., |D_v|\}\), with \(D_v(0)\) = 0 kW. We will also define the following set, which includes all charging arcs representing charging at location \(v\) at time \(t\) charging at a rate that is greater than \(\delta_1\) but at most \(\delta_2\):
\[
\mathcal{A}_S^{v, t, \delta_1, \delta_2} = \{(v, w) \in \mathcal{A}_S : v_v = v, t_v = t, \delta_1 \leq \frac{(c_w - c_v)E_c}{\Delta t} \leq \delta_2\}
\]
In this example, consider a location \(v\) with the option to install charging stations of three charging rates: \(D_v = \{7.7\text{ kW}, 16.8\text{ kW}, 50.0\text{ kW}\}\). Only the 50.0 kW station can charge at the rates from \(16.8\text{ kW}, 50.0\text{ kW}\), thus the constraint on charging flows with charging rates in this range is:
\[
\sum_{(v, w) \in \mathcal{A}_S^{v, t, 16.8, 50.0}} f(v, w) \leq S_{(v, 50.0)}
\]
Following, the constraint on charging flows with rates in \((7.7\text{ kW}, 16.8\text{ kW})\] is given by the number of plugs of the 16.8 kW station plus any unused plugs at the 50.0 kW station:
\[
\sum_{(v, w) \in \mathcal{A}_S^{v, t, 7.7, 16.8}} f(v, w) \leq \bar{S}_{(v, 16.8)} + (\bar{S}_{(v, 50.0)} - \sum_{(v, w) \in \mathcal{A}_S^{v, t, 16.8, 50.0}} f(v, w))
\]
Similarly, the constraint for flows with rates in \((0\text{ kW}, 7.7\text{ kW})\] is given by:
\[
\sum_{(v, w) \in \mathcal{A}_S^{v, t, 0.0, 7.7}} f(v, w) \leq \bar{S}_{(v, 7.7)} + (\bar{S}_{(v, 50.0)} - \sum_{(v, w) \in \mathcal{A}_S^{v, t, 7.7, 16.8}} f(v, w)) + (\bar{S}_{(v, 16.8)} - \sum_{(v, w) \in \mathcal{A}_S^{v, t, 16.8, 7.7}} f(v, w))
\]
After collecting like terms, the general form of the equations that determine charging station sizing are:
\[
\sum_{j=1}^{|D_v|} \left( \sum_{(v, w) \in \mathcal{A}_S^{v, t, D_v(j)}} f(v, w) - \bar{S}_{(v, D_v(j))} \right) \leq 0 \quad (2)
\]
\[
\forall j \in \{1, ..., |D_v|\}, \forall v \in V_R, \forall t \in T
\]
f) E-AMoD model with station siting: The cost terms that are considered in the E-AMoD problem are fleet procurement, charging station procurement, electricity (both energy consumption and demand charges), and vehicle maintenance. We seek to jointly solve for the vehicle flows \((f(v, w))\) \(\forall (v, w) \in \mathcal{A}\) and charging station sizing
\[ S_{*} \quad \forall s = (v, \delta) \in S, \forall v \in V_{R}, \forall \delta \in D_{v}, \text{such that total fleet costs are minimized:} \]

\[
\begin{align*}
\text{minimize} & \sum_{(v,w) \in A_{S}} f(v, w) (c_{w} - c_{v}) E_{c} p_{\text{energy}}(t_{v}) \quad (3a) \\
& + \sum_{v \in V_{R}} p_{\text{demand}}^{\text{max}} p_{\text{demand}} \\
& + \sum_{(v,w) \in A_{T} \setminus A_{T}} f(v, w) d_{v,\delta} p_{\text{dist}} \\
& + \sum_{\delta} n_{\text{fleet}} p_{\text{fleet}} \\
& + \sum_{v \in V_{R}, j=1} \bar{S}_{v}(v, D_{v}(j)) p_{\text{stn}}(D_{v}(j)) \\
\text{subject to} & \quad \sum_{(v,w) \in A_{T} \setminus A_{T}} A^{\text{in}}[v_{2}, t-1; :] f = -A^{\text{out}}[v_{2}, t-1; :] f \\
& \quad A^{\text{in}}[v_{1}, :] f = -A^{\text{out}}[v_{1}, :] f \\
& \quad \sum_{(v,w) \in A_{S}} f(v, w) E_{c} (c_{w} - c_{v}) E_{c} \Delta t \\
& \quad \leq p_{\text{max}}^{\text{max}} \forall v \in V_{R}, \forall t \in T \\
& \quad \text{Eq. (2)}
\end{align*}
\]

Objective term (3a) is the electricity energy cost, with time-varying electricity price \( p_{\text{energy}}(t) : T \rightarrow R^{+} \) having units of USD/kWh. Objective term (3b) is the electricity demand cost, with demand charge \( p_{\text{demand}} \in R^{+} \) having units of USD/kWh. Maximum power demand at each location \( p_{\text{max}}^{\text{max}} \) is defined from \( f \) in Eq. (3j), which follows from the derivation of Eq. (1). Objective term (3c) is the maintenance cost due to vehicle travel, with \( p_{\text{stn}} \in R^{+} \) representing maintenance cost per distance traveled and has units of USD/km. Objective term (3d) is the fleet procurement cost, with vehicle price \( p_{\text{fleet}} \in R^{+} \) having units of USD/vehicle. Fleet size \( n_{\text{fleet}} \in R^{+} \) is defined from \( f \) in Eq. (3f). Lastly, objective term (3e) is the charging station procurement cost, with \( p_{\text{stn}}(\delta) : D_{v} \rightarrow R^{+} \) having units of USD/station.

We introduce \( A \in R^{|V|} \times R^{|A|}, \) the incidence matrix of the expanded graph \( G, \) in which +1 entries indicate into node and -1 indicates out of node. \( A^{\text{out}} \) is the incidence matrix with only the -1 entries, whereas \( A^{\text{in}} \) is the incidence matrix with only the +1 entries. We denote \( A[V_{t}, :] \) as the selection of all columns and the rows corresponding to nodes in \( V_{t}, \) in which \( V_{t} \) is defined as the set of all expanded graph nodes associated with time \( t. \) Similarly, \( V_{t_{1} : t_{2}} \) returns the set of expanded graph nodes associated with a range of times, from \( t_{1} \) to \( t_{2}. \)

Eq. (3g) enforces the fleet to serve all customer travel requests. Eq. (3h) enforces consistency and flow conservation in the network flow problem, as detailed in [4] and [5]. Eq. (3i) enforces a periodicity constraint, ensuring vehicles return to a state in the final time that is identical to its state in the initial time. Eq. (3k) determines the station sizing \( S_{*} \) and enforces station plug capacities, as derived in Eq. (2).

The E-AMoD problem Eq. (3) is a linear program that is amenable for any general LP solver. It has \(|A_{R}| |C| |T| + |V_{R}| |D_{v}| + |V_{R}| + 1 \) decision variables. The dominant term is \(|A_{R}| |C| |T| \). Given that \( A_{R} \) can be at most \(|V_{R}|^{2} \) if there is a route between every location, it follows that \(|A_{R}| \leq |C| |T| \). A(\( O(|V_{R}|^{2}|C| |T|). \)

A few comments are in order. First, the transportation graph \( G_{R} \) uses routes between destinations as arcs, as opposed to road segments. The advantage of this modeling choice is that origin-destination travel demand data sets, with data on the traffic volume, distance, and travel time of the route connecting an origin-destination pair, can be readily used to formulate this graph; no assumptions are needed about how a vehicle traverses physical road segments in its routing. The disadvantage of this approach is that traffic congestion along road segments cannot be accurately modeled. However, if road topography data is available and shortest-path routing can be assumed, then Eq. (3) can easily be adapted to use road segments and enforce threshold congestion constraints in the optimization, as presented in [5]. Second, the flow solved by Eq. (3) allows for fractional flows of vehicles. However, this is acceptable given the macroscopic nature of the station siting problem, as arc flows are on the order of thousands of vehicles and a fractional vehicle has negligible impact on results. Third, although the number of decision variables scales with \( O(|V_{R}|^{2}|C| |T|) \), if the operating region of the fleet remains fixed, increasing the number of locations will increase the spatial granularity which requires a finer charge and time discretization. In such a case, the scaling would be more than quadratic with the number of locations.

III. CASE STUDY IN SAN FRANCISCO, CA

A. Model parameters

To investigate how charging stations are sited when optimized jointly with E-AMoD fleet operations, we conduct a detailed case study of an E-AMoD system in San Francisco, CA. The fleet operates for 24 hours, serving all travel demand in the city on a typical weekday. The fleet additionally serves San Francisco customers traveling to and from North Bay, East Bay, and the Peninsula. The fleet operator installs charging stations within San Francisco at which fleet vehicles have exclusive use for recharging; these installations are determined by the joint charging station siting optimization. To evaluate the impact of the vehicle battery size and efficiency, we conduct separate optimizations for the following three EV models: the 2020 Tesla Model 3 Long Range AWD (75 kWh battery), the 2020 Nissan Leaf S (40 kWh), and the 2021 Dacia Spring (27.4 kWh).

a) Data for expanded graph: We use travel demand data provided by StreetLight Data from 2019, averaged across Mondays-Fridays. The hourly origin-destination data is given for the 190 transportation analysis zones (TAZ) of
San Francisco [12] and three pass-through zones measuring traffic flow across the Golden Gate Bridge (to/from North Bay), the Bay Bridge (to/from East Bay), and all roads connecting the southern city boundary to the Peninsula. The 190 TAZs are then aggregated into 25 city zones determined by dividing San Francisco into a 5x5 grid of 2.2 km x 2.2 km cells. With 25 city zones and three pass-through zones, we have $|\mathcal{V}_R| = 28$. In total, the E-AMoD serves 2.89 million customer requests over the weekday. The distance and travel time between origin-destination pairs are also given by the data set. To account for the travel that occurs beyond the city boundaries, we add 32 km, 24 km, and 48 km to the distance and 40 min, 20 min, and 45 min to the travel time for vehicles traveling to or from the North Bay, East Bay, and Peninsula pass-through zones, respectively.

To determine the energy needed to travel between an origin-destination pair, we assume the EVs consume energy at the rate of their combined cycle energy efficiency rating, as rated by the US Environmental Protection Agency (EPA) for the Model 3 and Leaf S and the World harmonized Light-duty vehicles Test Procedure (WLTP) for the Spring. These ratings are provided in Table I. We can then determine travel energy directly from the travel distance data.

The 24-hour horizon is discretized into fifteen-minute time steps, such that $|T| = 96$. This time discretization was chosen to be close to the travel time of the shortest duration trip requests. It is also consistent with the frequency at which power is metered by the electric utility, which is how the utility determines energy and demand charges. We assume the hourly travel demand is uniformly distributed over the hour. For example, if the number of customer requests from 07:00 to 08:00 is 1000 for a particular origin and destination pair, we assume the number of requests at the time steps 07:00, 07:15, 07:30, and 07:45 to be 250.

We conservatively assume the EVs operate with their SoC between 0.2 and 0.8. This simple policy accounts for having emergency reserve battery charge, avoiding battery degradation effects at high SoCs [13], and the capacity loss of the battery over its usage. The SoC-restricted vehicle battery is then discretized into energy steps of 0.74 kWh, such that $|C| = 62, 33, 23$ for the Model 3, Leaf S, and Spring, respectively. This charge discretization was chosen to be close to the travel energy of the lowest energy trip requests.

The fleet operator can install charging stations at any of the 25 city zones. There are four different station options with varying charging rates: two Level 2 AC options, 7.7 kW and 16.8 kW, and two DC fast charging options, 50 kW and 150 kW. These options were chosen from common station configurations used in present day [14]. However, as the Spring has a smaller battery, the maximum charging rate it can receive is 30 kW. Thus, for the Spring optimization, although DC fast charging stations are considered, their output charging rates are limited to 30 kW. All EVs are assumed to recharge with a grid-to-battery efficiency of 90%.

b) Pricing data: We set the per-distance maintenance cost of EV travel to $p_{\text{maint}} = 0.0464 \, \text{USD/km} \times (0.0746 \, \text{USD/kWh})$ in accordance with the American Automobile Association (AAA)[15].

For electricity pricing, we use the “Business Electric Vehicle” electric schedule from Pacific Gas and Electric Company (PG&E), the primary electric utility that serves San Francisco [16]. This schedule consists of a time-of-use (TOU) rate, $p_{\text{energy}}(t)$, a price per unit energy that varies by time of day, and a subscription-based demand charge, $85.98 \, \text{USD/kWh}$, a price per unit power of maximum load within a billing month. The TOU rate, shown in Fig. 3, features a super-off-peak rate of $0.1032 \, \text{USD/kWh}$ from 9 am to 2 pm to incentivize energy use during midday peak solar production on the California grid, and a peak rate of $0.3347 \, \text{USD/kWh}$ from 4 pm to 9 pm to disincentivize energy use during peak grid load. As we are solving a macroscopic planning problem, we assign demand charges at the city zone level and make the demand charge continuous (instead of per 50 kW discretization) since the peak demand per zone is on the order of thousands of kilowatts. This monthly demand charge is then appropriately rescaled for the case study time horizon (24 hours) such that $p_{\text{demand}} = 0.056497 \, \text{USD/kWh}$.

In determining the per-vehicle fleet procurement cost, $p_{\text{fleet}}$, we assume a depreciation rate of 20%/year on the original sale price. Sale prices are provided in Table I. We also add an annual cost of $2127 \, \text{USD/vehicle}$ which includes the cost of insurance, registration, and finance charges [15].

This yearly cost is then rescaled for the case study time horizon such that $p_{\text{fleet}} = 20.09, 23.12, \text{and } 31.55 \, \text{USD/vehicle}$ for the Spring, Leaf S, and Model 3, respectively.

The per-station costs for charging station installation are $2887 \, \text{USD}, 3287 \, \text{USD}, \text{and } 8818 \, \text{USD}$ for the 7.7 kW, 16.8 kW, 50 kW, and 150 kW stations, respectively, based on Exhibit 1 of [14]. Assuming a station lifetime of 10 years, we can compute the equivalent annual cost and then rescale for the case study time horizon to obtain $p_{\text{stn}}(7.7 \, \text{kW}) = 2.61 \, \text{USD/station}, p_{\text{stn}}(16.8 \, \text{kW}) = 3.55 \, \text{USD/station}, p_{\text{stn}}(50 \, \text{kW}) = 13.36 \, \text{USD/station}, \text{and } p_{\text{stn}}(150 \, \text{kW}) = 41.37 \, \text{USD/station}$. Note that this cost accounts for the procurement of charging station equipment, cables, and accompanying transformers, but does not include costs associated with land use, labor, and permitting, which vary significantly by site.

B. Experimental design

Using the model parameters outlined in Section III-A, we conduct two experiments:

1) A comparison of E-AMoD fleet operations and station siting determined by joint optimization Eq. (3) between different fleet vehicle choices: the Model 3 (75 kW), the Leaf S (40 kW), and the Spring (27.4 kW).

2) A comparison of E-AMoD fleet operations and station siting determined by joint optimization Eq. (3) versus a “baseline” scenario in which an E-AMoD fleet optimizes operations on a fixed station siting based on present-day stations. For this comparison, the middle-sized EV, the Leaf S, is used.
TABLE I: Comparison of specifications, total costs, and charging results between EV models of varying battery size. The Dacia Spring fleet has the lowest total cost due to its high efficiency and low vehicle price.

| Unit                      | Model 3 | Leaf S | Spring |
|---------------------------|---------|--------|--------|
| Vehicle price USD         | 49,900  | 31,600 | 26,058 |
| Efficiency Wh/km          | 173     | 189    | 119    |
| Battery size kWh          | 40      | 40     | 27.4   |
| Fleet size                | 154.7k  | 154.7k | 154.7k |
| Fleet procurement cost USD| 4883.82k| 3579.49k| 3109.79k|
| Charging station cost USD  | 118.67k | 137.15k| 95.56k |
| Electricity cost kWh      | 721.01k | 774.03k| 540.74k|
| Electricity cost (demand charges) USD | 22.30k | 26.19k | 18.18k |
| Rebalancing cost USD      | 81.10k  | 81.20k | 77.77k |
| Total USD                 | 5826.90k| 4598.06k| 3842.05k|
| Charging energy MWh       | 6039.46 | 4883.30 | 8243.70 |
| Peak charging load MW     | 394.72  | 463.51 | 321.86 |
| Rebalancing distance traveled km | 1749.63 | 1751.80 | 1677.80 |

In the baseline scenario comparison, we determine the charging station siting from the US Department of Energy’s Alternative Fuels Data Center (AFDC) API. The API returns the number of Level 2 and DC fast charging plugs for every recorded charging station in San Francisco. We assume Level 2 stations are 7.7 kW and DC fast charging stations are 50 kW, which are common charging rates currently used. As EV penetration is much lower in present day compared to our joint optimization future mobility scenario in which all travel is served by EVs, we scale up the present-day station distribution by a constant factor of 59.86 such that the city total installed charging infrastructure capacity is equal to the total installed capacity resulting from the joint optimization, 629.91 MW.

C. Results and discussion

a) Comparison between EV models: A summary of results for the comparison between EV models is presented in Table I.

Fleet procurement cost is the most significant cost term, accounting for 77.8% to 83.8% of total costs. For all EV models, the optimization prioritizes having the fewest number of vehicles possible to satisfy peak travel demand and any necessary rebalancing between trips. As a result, the number of vehicles determined by the optimization is identical for all EV models, with \( n_{\text{fleet}} = 155.77 \) k.

Energy electricity cost is the second largest cost term for all three EV models, accounting for 12.4% to 16.8% of total cost. As shown in Fig. 3, the E-AMoD fleet has sufficient charge scheduling flexibility to completely avoid charging during the highest price period from 4 pm to 9 pm. Conversely, the fleet’s peak charging occurs during the lowest price period from 9 am to 2 pm.

The given travel demand also plays a key role in determining charge scheduling and station siting. The macroscopic pattern in the San Francisco transportation system is for vehicles to begin the day primarily in the non-commercial zones, then concentrate in the downtown commercial district (Zones 4, 5, 9, and 10; see map in Fig. 2) in the morning rush hour between 7 am and 9 am, then return to the non-commercial zones in the evening rush hour between 4 pm and 6 pm. The temporal aspect of this travel pattern can be seen in the passenger-carrying vehicles of Fig. 1. As a result, there is a longer period of charging primarily in non-commercial zones from after the evening rush hour to the morning rush hour of the following day, and a shorter 8-hour period during the midday working hours between the rush hours in the commercial zones. Given the high number of vehicles in the commercial zones in the midday, a low electricity price, and a short window in which these vehicles are concentrated there, the optimization installs a greater number of stations in the commercial zones, shown for the Leaf S in Fig. 2a. For the Leaf S, 50 kW DC fast charging stations are installed at these commercial zones to ensure vehicles can quickly recharge within this midday period before the evening rush hour. While the Model 3 and Spring also have greater installed capacity in the commercial zones, no DC fast charging is installed in any of the zones for either EVs, as seen in Fig. 4a (however, recall that fast charging above 30 kW is not an option for the Spring). With an 87.5% larger battery, the Model 3 does not require as much recharging at midday as the Leaf S to make it through the evening rush hour (and the high electricity price period). Despite having a smaller battery, the light-weight Spring is 37.0% more efficient than the Leaf S and also requires less midday recharging.

The advantage of the Spring’s higher efficiency is impactful across every cost term, and furthermore, reduces load in both the power and transportation systems. In comparison with the larger battery EV models, the Spring consumes less energy and consequently requires less installation of charging infrastructure, has a lower peak charging load, and fewer vehicle miles travelled (VMT) due to less rebalancing travel needed to load balance charging demand between stations. However, in further experiments with yet smaller EV models (not shown in the interest of space limitations), a trade-
Fig. 2: (a) Heat map of installed charging capacity resulting from the siting optimization with the Leaf S fleet. (b) Heat map of the difference in installed charging capacity for a Leaf S fleet between the joint charging station siting optimization scenario and the baseline siting scenario. Red indicates greater installed capacity in the optimized scenario whereas blue indicates greater capacity in the baseline scenario.

Fig. 3: (a) Comparison of total charging load between fleets of varying EV models. (b) Comparison of total charging load for Leaf S fleet between optimized station siting and baseline station siting scenario. In both figures, the TOU electricity price is plotted against the right axis.

Table II: Comparison of total costs and charging results for the Leaf S fleet between an optimized charging station scenario and the baseline scenario.

|                      | Unit   | Leaf S, Baseline | Leaf S, Optimized | Change  |
|----------------------|--------|------------------|-------------------|---------|
| Fleet size           | USD    | 154.77k          | 154.77k           | 0.00%   |
| Charging station     | USD    | 199.10k          | 137.15k           | −31.11% |
| procurement cost     | energy | 806.92k          | 774.03k           | −4.08%  |
| Electricity cost,    | energy | 29.12k           | 26.19k            | −10.07% |
| demand charges       | USD    | 91.44k           | 81.20k            | −11.20% |
| Rebalancing cost     | USD    | 1126.57k         | 1018.57k          | −9.59%  |
| Total                | USD    | 1126.57k         | 1018.57k          | −9.59%  |
| Charging energy      | MWh    | 6819.27          | 6521.18           | −4.37%  |
| consumed             | Peak charging | 515.42         | 463.51            | −10.07% |
| load                 | Rebalancing | 1972.65         | 1751.80           | −11.20% |
| distance traveled    | km     |                  |                   |         |

TABLE II: Comparison of total costs and charging results for the Leaf S fleet between an optimized charging station scenario and the baseline scenario.
city zones by installed charging capacity (16% of all zones), which are the commercial zones, already make up 74% of the total installed capacity. In contrast, it requires the top 13 stations (52% of all zones) in the optimized siting scenario to attain that same share of capacity. The present-day siting is justifiable given low EV penetration and no automation, since it captures charging business in high traffic regions at times of day when people are active. However, in a future mobility scenario with a high penetration of E-AMoD, the optimal siting is spread more uniformly throughout the city. Consequently, rebalancing VMT is reduced by 11.20% as less repositioning is required for vehicles to access available charging stations, which in turn contributes to a 4.08% reduction in energy consumption and a 10.07% reduction in peak charging load, as shown in Table II. Additionally, as the fleet vehicles are autonomous and can operate at all hours of the day, they are not limited to charging during the midday when there is a large share of vehicles in the commercial zones. The ability for vehicles to autonomously take turns recharging in the middle of the night, when they are largely in non-commercial zones, allows for greater distribution of charging throughout the day and a lower peak load in the joint optimized scenario, as shown in Fig. 3b. Notably, there is a 64% reduction in installed DC fast charging capacity in favor of high-power Level 2 AC charging.

The joint optimization problem Eq. (3) for the Leaf S fleet, which has 5.3 million decision variables, was solved using Gurobi solver in 61 iterations over 2.33 hours on a compute instance with 24 vCPU and 64GB RAM.

IV. CONCLUSION

This paper explored the benefits of optimizing the operations of a fleet of electric Autonomous Mobility-on-Demand (E-AMoD) vehicles jointly with the siting of the charging infrastructure. In particular, we devised a network flow model capturing the movements and charging activities of the electric vehicles (EVs) in time, and integrated it within the static charging infrastructure siting problem. The resulting joint design and control problem is convex and can be solved to global optimality with off-the-shelf linear programming algorithms. Our real-world case-studies compared the total costs achievable with three different types of EVs, revealing that the lightest and cheapest EV, despite its limited range, would result in the lowest total cost, and that changing the vehicle type would significantly affect the resulting infrastructure design. Finally, we quantified the benefits of jointly optimizing the siting of the chargers. Our results revealed that, compared to the case where the infrastructure siting corresponds to a linear scale-up of the present-day layout and only the E-AMoD operations are optimized, our joint optimization framework can reduce the total cost incurred by the E-AMoD operator, the peak charging load, and the empty-vehicle distance traveled by up to 10%, and also lower the charging station procurement cost by more than 30%. In particular, the share of charging capacity provided by DC fast charging stations is reduced nearly three-fold in favour of high-power Level 2 AC stations.

This work can be extended as follows: First, we would like to capture the effects of EV charging on the power grid, potentially jointly optimizing its design and enabling vehicle-to-grid operations. Second, it is of interest to study the impact of heterogeneous fleets consisting of differently sized EVs, and of hybrid electric and internal combustion engine vehicles. Finally, we would like to investigate the sensitivity of our results with respect to travel demand variability and different energy consumption models.

ACKNOWLEDGMENTS

J. Luke would like to thank StreetLight Data, Inc. for providing travel demand data of San Francisco under the StreetLight Academic Access Agreement. The authors thank Dr. Ilse New and Dr. Edward Schmerling for proofreading this paper. This research was supported by the National Science Foundation under the CPS program and the Stanford University Bits & Watts EV50 Project. This article solely reflects the opinions and conclusions of its authors and not NSF or Stanford University.

REFERENCES

[1] K. Palmer, J. E. Tate, Z. Wadud, and J. Nellthorp, “Total cost of ownership and market share for hybrid and electric vehicles in the uk, us and japan,” Applied energy, vol. 209, 2018.
[2] K. Spieser, K. Treleaven, R. Zhang, et al., “Toward a systematic approach to the design and evaluation of Autonomous Mobility-on-Demand systems: A case study in Singapore,” in Road Vehicle Automation, Springer, 2014.
[3] A. B. Styczynski and L. Hughes, “Public policy strategies for next-generation vehicle technologies: An overview of leading markets,” Environmental Innovation and Societal Transitions, vol. 31, 2019.
[4] F. Rossi, R. Iglesias, M. Alizadeh, and M. Pavone, “On the interaction between Autonomous Mobility-on-Demand systems and the power network: Models and coordination algorithms,” IEEE Transactions on Control of Network Systems, vol. 7, no. 1, 2020.
[5] A. Estandia, M. Schiffer, F. Rossi, et al., “On the interaction between autonomous mobility on demand systems and power distribution networks – an optimal power flow approach,” IEEE Transactions on Control of Network Systems, 2021.
[6] F. Boewing, M. Schiffer, M. Salazar, and M. Pavone, “A vehicle coordination and charge scheduling algorithm for electric autonomous mobility-on-demand systems,” in American Control Conference, In press, 2020.

[7] R. Roberti and M. Wen, “The electric traveling salesman problem with time windows,” English, Transportation Research. Part E: Logistics and Transportation Review, vol. 89, 2016, ISSN: 1366-5545.

[8] T. D. Chen, K. M. Kockelman, M. Khan, et al., “The electric vehicle charging station location problem: A parking-based assignment method for seattle,” in Transportation Research Board 92nd Annual Meeting, vol. 340, 2013.

[9] L. Jia, Z. Hu, Y. Song, and Z. Luo, “Optimal siting and sizing of electric vehicle charging stations,” in 2012 IEEE International Electric Vehicle Conference, 2012.

[10] H. Zhang, S. J. Moura, Z. Hu, and Y. Song, “Pev fast-charging station siting and sizing on coupled transportation and power networks,” IEEE Transactions on Smart Grid, vol. 9, no. 4, 2018.

[11] K. M. Tan, V. K. Ramachandaramurthy, and J. Y. Yong, “Integration of electric vehicles in smart grid: A review on vehicle to grid technologies and optimization techniques,” Renewable and Sustainable Energy Reviews, vol. 53, 2016.

[12] Metropolitan Transportation Commission. (2018). “Transportation analysis zones.” Available at http://opendata.mtc.ca.gov/datasets/transportation-analysis-zones.

[13] B. Lunz, Z. Yan, J. B. Gerschler, and D. U. Sauer, “Influence of plug-in hybrid electric vehicle charging strategies on charging and battery degradation costs,” Energy Policy, vol. 46, 2012.

[14] C. Nedler and E. Rogers, “Reducing ev charging infrastructure costs,” Rocky Mountain Institute, Tech. Rep., 2020, Available at https://rmi.org/wp-content/uploads/2020/01/RMI-EV-Charging-Infrastructure-Costs.pdf.

[15] American Automobile Association. (2020). “Your driving costs.” Available at https://newsroom.aaa.com/wp-content/uploads/2020/12/2020-Your-Driving-Costs-Brochure-Interactive-FINAL-12-9-20.pdf.

[16] Pacific Gas and Electric Company. (2020). “Electric schedule bev.” Available at https://www.pge.com/tariffs/assets/pdf/tariffbook/ELEC_SCHEDS_BEV.pdf.