Security of classical noise-based cryptography

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We examine the security of a protocol on cryptographic key distribution proposed by Yuen and Kim (1998 Phys. Lett. A 241 135). Theoretical and experimental analysis shows that, even if the eavesdropper could receive more photons than the legitimate receiver, secure key distribution is possible as long as the signal-to-noise-ratio of the eavesdropper does not exceed eight times (9 dB) that of the receiver. Secure key distribution was demonstrated using conventional fiber optics. The secure key transmission rate in the experiment was estimated to be 2 Mb/s at its maximum (0.04 bit per sender’s bit.) The present protocol has advantages over other quantum key distribution protocols in that it is more efficient and more easily implemented, but careful design and management are necessary to ensure the security of the cryptosystem.

I. INTRODUCTION

Cryptography is used to transmit a message from a sender (referred to as Alice) to a receiver (Bob) without leaking useful information to others. It has been proved that a message can be transmitted securely if it is coded and decoded by a sequence of random bits (key) whose length is equal to that of the message. The problem of secure transmission is then reduced to that of generating a secret key shared by Alice and Bob. Classical cryptosystems rely on computational complexity and may be broken by an effective algorithm or a powerful computer. Quantum key distribution (QKD) protocols, in contrast, provide an unconditionally secure key, the security of which is inherent in the laws of quantum mechanics. This remarkable advantage of QKD protocols has been attracting increasing research interest [1–5] since the proposal by Bennett and Brassard [1]. Although QKD has been demonstrated in over-20-km-fiber communication channels [6–10], its application in practical communication systems is not straightforward. The QKD protocols require single-photon transmission to guarantee the security, and thus are vulnerable to loss and noise inherent in actual transmission channels. Optical amplifiers will not solve this problem, because the noise of the optical amplifiers inevitably destroys the quantum correlation. Single-photon transmission requires the use of complicated and inefficient photon counting techniques instead of conventional analog detection, besides a truly practical single-photon source is not yet available. The QKD protocols are therefore not fully compatible with the current optical fiber communication systems. A secure key distribution protocol compatible with the current systems is desirable. This would be a protocol that uses more than one photon and allows optical amplifiers to be used. Such a protocol would be based on coherent state photons, or classical light.

Maurer [11] has shown perfect cryptographic security can be obtained in a classical noisy channel with the help of a noiseless feedback channel. Yuen and Kim [12] examined the principles underlying the QKD protocol with two non-orthogonal quantum states (B92 protocol [4].) The security of the B92 protocol relies on two facts [4]: (i) an eavesdropper (Eve) cannot accurately determine the value of each transmitted bit (i.e., no efficient opaque eavesdropping.) (ii) Eve cannot closely correlate Bob’s measurement results with her own (i.e., no efficient translucent eavesdropping.) Yuen and Kim [12] pointed out that these two conditions can be satisfied in a classical transmission system, where the detectors of Bob and Eve are under independent additive noise and show a small signal-to-noise-ratio (SNR.) They proposed a classical noise-based protocol for key distribution (referred here to as the YK protocol.) The YK protocol working with classical light, would have advantages in practical implementations. Proving the security in YK protocol is, however, subtler than in QKD protocols. Since many photons are transmitted to carry one-bit information, the conditions specified above will not be satisfied if the SNR of Eve’s detection is sufficiently high. Eve’s SNR can be increased by using low-noise detection equipment, or simply by moving closer to Alice than Bob (because of the fiber loss.) The original analysis of the security of YK protocol assumed the same SNR for Bob and Eve [12]. For practical implementations, it is important to determine the design rules of Eve’s SNR and Bob’s.

In this article we quantitatively examine the security of the YK protocol, and show that the YK protocol is secure, even if Eve’s SNR is 9 dB better than Bob’s. We also show experimental results that demonstrate secure key distribution against translucent attack. Section 2 provides the condition for secure key distribution in terms of the
secure key distribution rate. Section 3 describes the experiment on the YK protocol using conventional fiber optics. Section 4 discusses the implementation issues.

II. THEORY

We first define the secure key distribution rate. Suppose Alice transmits an equally probable binary string to Bob. Shannon information between Alice and Bob is expressed by

\[ I_{AB} = 1 + e_B \log_2 e_B + (1 - e_B) \log_2 (1 - e_B), \]

where \( e_B \) denotes the error rate of Bob’s decision. Because of the decision errors, Bob has the information in only \( n_{sift} t_{AB} \) of the \( n_{sift} \) sifted bits. Alice and Bob exchange redundant information over the public channel in order to obtain the reconciled key. This procedure is called error correction, the best known practical protocol for which was given by Brassard and Salvail [14]. For successful error correction with Brassard-Salvail’s protocol, the error rate should be less than 0.15. To establish a secret key, Alice and Bob use privacy amplification [14], random hashing of the reconciled key into a shorter key. If they shorten the reconciled key of length \( n_{rec} \) by the fraction \( \tau \) and sacrifice \( n_S \) bits as a safety parameter, Eves’s Shannon information on the final key of length \( \tau n_{rec} - n_S \) is bounded by

\[ I_E \leq \frac{2^{-n_S}}{\ln 2}. \]

The fraction \( \tau \) is given by

\[ \tau = 1 + (1/n_{rec}) \log P_C, \]

where the collision probability \( P_C (X) \) of \( X \) is defined as follows: Let \( X \) be a random variable with an alphabet \( X \) and distribution \( P_X \). The collision probability is the probability that \( X \) takes the same value twice in two independent experiments, that is, \( P_C (X) = \sum_{x \in X} P_X (x)^2 \). The logarithm of the collision probability thus refers to Eve’s information on the key. The collision probability can be expressed by the probability \( p(k) \) that \( k \) is the \( i \)-th signal of Bob’s string and the joint probability \( p(k, l) \) that \( k \) is the \( i \)-th signal of Bob’s string and \( l \) is the \( i \)-th signal of Eve’s string. We have the following formula [14] for the fraction \( \tau \):

\[ \tau = 1 + \log_2 \left[ \sum_{k, l} \frac{p(k, l)^2}{p(k)} \right]. \]

According to Bruß and Lütkenhaus [17], Bob can generate secure bits from his sifted bits at the rate \( R \) of

\[ R = I_{AB} - (1 - e_B) \tau - e_B. \]

We refer this rate \( R \) as the secure key distribution rate, and for secure key distribution its value be positive. The actual key generation rate is further reduced by multiplying the generation rate of the sifted key. In the following part of this section, we derive the conditions under which \( R \) is positive.

In the YK protocol [14], the bit values (“0” and “1”) are encoded so as to make the probability distribution of the received signal symmetric. Alice sends encoded bits on a weak classical light. Signal \( s_0(t) = S \phi(t) \) is transmitted for “0”, and \( s_1(t) = -S \phi(t) \) is transmitted for “1”, where \( \int_{-T}^{T} \phi(t)dt = 1 \). We here measure the signal value as the voltage on the load resistance \( R_{load} \) of a photodiode. Mean signal voltage \( S \) is defined by \( S^2 = \int_{-T}^{T} s_0^2 (t)dt \), and \( S^2/R_{load} \) represents the signal energy over the duration \( T \) (signal energy per bit.) The output \( r(t) \) of the detector contains the noise \( u(t) \), so \( r(t) = s_i(t) + u(t) \). If the noise is white Gaussian noise with spectral density \( \sigma^2 \), the probability distribution of the detected signal \( V \) is expressed by

\[ P(V) = \begin{cases} \left(\frac{1}{\sqrt{2\pi}}\right) \exp \left[ -\frac{(V - S)^2}{2\sigma^2} \right] & \text{for “0”} \\ \left(\frac{1}{\sqrt{2\pi}}\right) \exp \left[ -\frac{(V + S)^2}{2\sigma^2} \right] & \text{for “1”} \end{cases}, \]

where the signal is averaged over the duration \( T \) as \( V = \int_{-T}^{T} r(t)dt \). The SNR \( \beta^2 \) in this system is defined by \( \beta = S/\sigma \). In a conventional decision scheme the bit values are determined to be “0” if \( V > 0 \) and “1” if \( V < 0 \). Decision errors will occur at the rate of \( Q(\beta) \), where \( Q \) is the scaled complementary error function defined by
We set a threshold $V_{th} = mS (m > 1)$ to make a decision: “0” if $V > V_{th}$ and “1” if $V < -V_{th}$, but leave inconclusive if $-V_{th} \leq V \leq V_{th}$. The probability of making a decision is given by the following decision rate:

\[ F_{+} = Q((m + 1) \beta) + Q((m - 1) \beta), \]

and the error rate is

\[ e = \frac{Q((m + 1) \beta)}{F_{+}}. \]

The sifted key is generated from the raw bit string by the Bob’s decision. The decision rate $F_{+}$ thus refers to the generation rate of the sifted key. As seen in Eqs. (8) and (9), the decision rate $F_{+}$ and the error rate $e$ are determined by the values of the SNR and the threshold. As described below, this error rate determines the joint probabilities $p(k, l)$ and therefore the secure key distribution rate. The system is thus fully characterized by the SNR and the threshold.

As in the B92 protocol [5], the inconclusive results play a essential role in guaranteeing the security of the key distribution. A finite threshold value of Bob enables him to make accurate decisions on his sifted key at a cost of the generation rate. Eve, on the other hand, should make a decision with zero threshold in order to obtain conclusive results for all the transmitted bits. If Eve uses a finite threshold in her decision, she will obtain the inconclusive results on the sifted bits. The assumption of independent noise prevents Eve from predicting which bit Bob will obtain a conclusive result. Eve can acquire no information from these inconclusive bits. Since Eve’s error rate $e_E$ is less than 1/2, she will obtain more information by making a decision with zero threshold. Therefore, Bob can make more accurate decisions on the sifted key bits than Eve can. That is, Bob has more information than Eve, and can distill secure key bits with Alice.

Now we will examine the conditions for security against eavesdropping. We here consider only two simple kind of eavesdropping, translucent attack and opaque attack. A translucent attack can be made by simply putting a beam splitter in the transmission channel. The translucent attack to the YK protocol, in contrast to those to the QKD protocols, will not change the state of the transmitted light. The probability distribution of Bob’s bits is the same as that of Alice’s, $p(0) = p(1) = 1/2$, because after error correction Alice and Bob share completely correlated results. The joint probabilities $p(k, l)$ are $p(0, 0) = p(1, 1) = (1 - e_E)/2$ and $p(0, 1) = p(1, 0) = e_E/2$. The fraction $\tau$ is calculated from Eq. (8) as

\[ \tau = 1 + \log_2 \left(1 - 2e_E + 2e_E^2\right). \]

The secure key distribution rate can be estimated by using Eqs. (8), (9), and (10). Figure 3 shows Eve’s required threshold and error rate as a function of Bob’s. As Bob’s error rate $e_B$ increases, Eve’s error rate should be increased in order to obtain a positive secure key distribution rate. For example, if Bob’s error rate is 0.15, Eve should make errors at a rate greater than 0.27. This implies that SNR of Eve’s system should be less than 0.38 for white Gaussian noise. On the other hand, Bob’s SNR should be better than 0.057 to keep his error rate smaller than 0.15 and his decision rate at $10^{-3}$. The secure key distribution is therefore possible even if Eve’s SNR is six times (8 dB) as large as Bob’s. The tolerance of the SNR increases as Bob’s error rate decreases, and it reaches 10 dB for $e_B = 0.01$.

In an opaque attack, Eve receives all the photons in $n\eta$ out of the $n$ bits sent by Alice. Then Eve sends the $n\eta$ bits to Bob according to her decision. Eve never touches the rest of the bits ((1 − $\eta$) $n$ bits) and forwards them to Bob. To protect information from opaque attack, Bob should determine his threshold according to the average signal intensity of each bit. If he observes only the average intensity over many bits, Eve can set a finite decision threshold to reduce her error rate and will then obtain conclusive results for $\gamma\eta m$ bits ($\gamma < 1$.) If she sends only the conclusive results with signals $\gamma^{-1}$ times as intense as received, Bob will obtain the same long-time average signal intensity he would if Eve did not intercept the photons. If Bob observes the signal intensity of each bit, Eve must send every bit with the same intensity as she receives it. Eve then should make a decision with zero threshold, otherwise she will lose the information on the inconclusive results. There is a trade-off for Eve on the fraction $\eta$: a large $\eta$ will increase Eve’s information gain, but will also make her easily detectable from the increase of Bob’s error rate. Bob’s error rate on the intercepted bits is $e_B$, but the error rate on the intercepted bits is $1 - e_E + e_E(1 - e_B)$. The eavesdropping thus increases Bob’s error rate to

\[ e'_B = (1 - \eta) e_B + \eta [(1 - e_E) e_B + e_E (1 - e_B)]. \]
To calculate the secure key distribution rate by using Eqs. (1), (5), and (10), we estimate the joint probabilities \( p(k,l) \). After the error correction, Bob has \((1 - \epsilon_B')nF_+\) bits. The probability distribution is symmetric: \( p(0) = p(1) = 1/2 \). Eve obtains \((1 - \epsilon_E)(1 - \epsilon_B)\eta nF_+ + (1/2)(1 - \eta)(1 - \epsilon_B)nF_+\) correct results and \( \epsilon_E\epsilon_B\eta nF_+ + (1/2)(1 - \eta)(1 - \epsilon_B)nF_+\) incorrect results on Bob’s bits. The joint probabilities are obtained as

\[
\begin{align*}
\quad p(1,1) & = \frac{[(1 - \epsilon_E)(1 - \epsilon_B)\eta + (1 - \epsilon_B)(1 - \eta)/2] nF_+}{2(1 - \epsilon'_B)nF_+} \\
\quad p(1,0) & = \frac{\epsilon_E\epsilon_B\eta nF_+ + (1 - \epsilon_B)(1 - \eta)nF_+/2}{2(1 - \epsilon'_B)nF_+} \\
\quad p(0,0) & = p(1,1) \\
\quad p(0,1) & = p(1,0).
\end{align*}
\]

Figure 4 shows the minimum required values of Eve’s error rate for secure key distribution \((R > 0)\) as a function of Bob’s error rate \( \epsilon_B' \). Though Bob can observe only \( \epsilon_B' \) values, he can estimate \( \epsilon_B \) from the SNR of his detection system. Eve will be detected if \( \epsilon_B' \gg \epsilon_B \). The detection is easy if Bob’s error rate is much lower than Eve’s. A high error rate for Bob may hide Eve, but secure key distribution is possible even in this case. Suppose \( \epsilon_B = 0.1 \) and \( \epsilon_B' = 0.15 \). As shown in Fig. 4, the secure key distribution rate is positive if Eve’s error rate is larger than 0.12. If the system is under white Gaussian noise, this condition on the error rate is satisfied when Eve’s SNR is smaller than 1.35 (1.3 dB). Since Bob’s SNR should be better than 0.089 (-10.5 dB) to keep the decision rate at 10, increasing the light intensity reduces Eve’s error rate, and makes the secure key distribution impossible.

### III. EXPERIMENT

In implementing the YK protocol, we should code the bit values in such a way that the probability distribution of the received signals is symmetric. In this experiment we used the unipolar Manchester code. This code represents "1" as a change from OFF to ON and "0" as a change from ON to OFF. It can be decoded as follows: divide the incident light into two paths, one of which is set one half of the pulse width longer than the other. Then take a difference as a change from ON to OFF and "0" as a change from OFF to ON. It can be decoded as follows: divide the incident light signal LD was set weaker than that of the trigger LD. The clock frequency in the present experiment was 25 MHz. Only a fixed pattern of 101010... was transmitted. The coded signal light then became a square wave with a duty of 50 % and a pulse duration of 20 ns. We sent strings of 30.8 kbits. The outputs of the two LDs were combined and attenuated by an attenuator (ATT1.) To simulate the translucent attack by an eavesdropper, we inserted a 50:50 fiber delay of a half pulse width, and a balanced detector. The balanced detectors made of two commercial InGaAs pin photodiodes loaded by 50 Ω resistors were operated in analog mode. The catalog data (typical values) for the quantum efficiency and the dark current of the photodiodes at 25 C were 90 % and 5 nA. The photodiodes were not cooled. The output signals of the receivers were led to amplifiers \((G = 40 \text{ dB})\) and then to analog-digital converters.

Figure 6 shows a typical probability distribution of the output signal from the amplifier. It is well represented by the sum of two Gaussians. The intensity of the optical signal was 0.380 μW (-34.2 dBm) at the input port of the receiver, and the SNR of this signal was 1.0 (0 dB.) We averaged the output pulse over the duration (10 ns), and evaluated the decision rate and error rate as a function of the SNR and the threshold. The results are shown in Fig. 6 and Fig. 7. The experimental results agree well with the theory assuming white Gaussian noise. These indicated that white Gaussian noise dominated the present receiver sensitivity, and that the security analysis described in Sec.
2 can be applied to the experiment. The number of the sifted bits became small when the threshold value is high. We had less than 30 bits, if the decision rate is less than $10^{-3}$. This insufficient sample number caused the error rate fluctuation observed for large $m$’s in Fig. 2. For SNR values up to 0 dB, the noise level was almost same as the dark noise level, but for larger SNR, it increased with the signal intensity. Dark current of the photodiodes was negligible compared to the thermal noise. These indicates that, for SNR values up to 0 dB, the sensitivity of the system was dominated by thermal noise, which is constant to the input photon number. As the intensity increased, the thermal noise was exceeded by shot noise, which is proportional to the input photon number. SNR was proportional to the square of the input power for weak signals, and tended to be proportional to the input power as the signal intensity increased.

The error rate shown in Fig. 2 provides a criterion for key distribution secure against opaque attack. A low error rate of 0.038 was obtained for weak signals by setting the threshold at $m = 10$, where the SNR was -9.25 dB. The decisions were made at the rate of 0.0008, slightly lower than $10^{-3}$. This error rate was lower than the theoretical value of 0.072 because of the fluctuation described above. Using $e_B = 0$ line in Fig. 4, we conclude that the key distribution is secure if Eve’s error rate is larger than 0.1, where we use the theoretical value of the error rate (0.072) for Bob. This condition is satisfied if Eve’s SNR is 0 dB, because we obtained the error rate of 0.15 in the experiment. Bob’s advantage in SNR was thus greater than 9.25 dB. This advantage was almost constant for large SNR signals.

Security against the translucent attack was examined as follows. We assigned one receiver that followed ATT2 as Bob, and the other receiver as Eve. ATT1 affected the SNRs of both Bob and Eve, whereas ATT2 determined the ratio of the SNRs. The decisions in Bob were recorded with several values of the threshold $m$, while the Eve’s decisions were recorded with the threshold fixed at zero. We measured the error rate $e_B$ and decision rate $F_k$ of Bob and the error rate $e_E$ of Eve. We estimated the joint probabilities $p(0,0)$, $p(0,1)$, $p(1,0)$, and $p(1,1)$ from the bit data about which Bob made correct decisions. Finally, we calculated the secure key distribution rate $R$ by using Eqs. (3), (4), and (5). Figure 3 shows the secure key distribution rate as a function of the error rates of Eve and Bob. The symbols in Fig. 3 show the secure key distribution rates estimated from the experiment. Experimental results agree well with theoretical results (lines.) The secure key distribution was achieved if error rates of Eve and Bob are in the region above the $R = 0$ line in Fig. 3. The decrease in Bob’s SNR reduced the range of the signal intensity for secure key distribution. Secure key distribution was impossible when Bob’s SNR was -9 dB smaller than that of Eve. This result also agrees well with the prediction. We obtained the largest actual secure key distribution rate $F_k R = 0.04$ when the SNRs of both Bob and Eve were unity (0 dB) and Bob’s threshold was set to $m = 2$. The observed error rates were 0.01 for Bob and 0.15 for Eve. The secure key distribution rate was $R = 0.29$. Higher secure key distribution rates were obtained by setting larger threshold values, but the reduction in the decision rate decreased the product $F_k R$. Alice transmitted signals at 50 Mb/s, so that the key transmission rate in the present experiment was 2 Mb/s. This is a hundred times as fast as the key transmission rate reported in the QKD experiments [6,10]. The transmission rate was limited only by the electric circuits. The secure key would be transmitted at 400 Mb/s if a 10-Gb/s transmission channel were used.

### IV. DISCUSSIONS

This theoretical analysis has shown that the secure key distribution is possible as long as the ratio of Bob’s SNR to Eve’s is better than -9 dB, and the experimental results presented here confirmed it. A practical cryptosystem should thus be designed to satisfy this condition. Eve may stay much closer to Alice than Bob, and her signal may be larger than Bob’s because of the fiber loss. We estimate a limit of the transmission distance in the following. It would be very difficult to use complicated networks, where the path of a traffic is not fixed. We have to construct a cryptosystem on a simple network or a point-point channel. Suppose, for simplicity, we construct it on a point-to-point channel. SNR is proportional to the square of the light intensity when the system sensitivity is limited by thermal noise. Then Bob’s advantage of 9 dB refers to the fiber length of 22.5 km using a lowest loss fiber (0.2 dB/km) and neglecting connection loss. SNR is proportional to the light intensity in systems limited by shot noise, and the fiber can be as long as 45 km in those systems. This values would be increased assuming the translucent attack, because Eve would tap the channel and receive small part of the signal.

Amplifiers can be used in YK protocol as long as the SNR permits. They will improve the SNR by reducing the effect of the thermal noise, and therefore will be useful when the system is limited by the thermal noise. In the shot noise limit, even an ideal amplifier reduces the SNR by 3 dB. The use of amplifiers is restricted by this degradation in the SNR. At most three amplifiers are thus possible.

The above estimation assumed that Bob and Eve use the same detectors. Bob should reduce system noise as possible to guarantee the security, by cooling the receiver, for example. If he can suppress all the thermal noise, the SNR of his system will be limited by shot noise, the standard quantum limit [18]. The mean photon number transmitted in this
system should be reduced to unity, because the SNR of 0 dB refers to mean photon number of unity in the shot noise limited systems. The error rate can be reduced below the standard quantum limit by optimum decision [19,20]. The improvement will be apparent for small mean photon numbers. Security analysis based on quantum detection theory as well as practical implementation of the optimum decision are open for further study. It would be noteworthy that the security analysis described in the present article will provide a security criteria for the B92 protocols employing dim coherent lights.

The YK protocol provides more efficient key distribution at higher bit rates than do other QKD protocols, but it requires that the signal intensity be controlled to keep Eve’s SNR advantage smaller than 9 dB. This may be a disadvantage compared to the QKD protocols like BB84, where the unconditional security is proved if the photons are generated by a perfect single photon source [21,22]. However, it has been shown [23] that the Eve’s advantage in SNR will limit the efficiency of the protocol in a lossy channel. The SNR control would be also required in actual BB84 systems.

V. CONCLUSION

Quantitative analysis of the security of the Yuen-Kim protocol shows that the secure key distribution is possible even if the eavesdropper receives signals with a signal-to-noise-ratio better than that with which the legitimate receiver receives them. It has been shown that the signal-to-noise-ratio of the legitimate receiver may be -9 dB smaller than that of the eavesdropper. The results of an experiment using conventional fiber optics agrees well with the analysis results. These results have demonstrated a practical implementation of a secure key distribution protected by the laws of physics. We think the YK protocol would be a solution for practical cryptography systems.
FIG. 2. Relation between threshold and the error rate obtained at various signal-to-noise-ratios. The meanings of the symbols are the same as in Fig. 1.

FIG. 3. The requirement for Eve’s error rate as a function of Bob’s error rate to achieve secure key distribution against translucent attack. Lines are calculated for the values of the secure key distribution rate \( R = 0, 0.1, 0.2, \) and 0.4. Symbols represent the secure key distribution rate obtained in the experiment. Crosses denote \( R < 0 \), diamonds: \( 0 < R < 0.1 \), triangles: \( 0.1 < R < 0.2 \), squares: \( 0.1 < R < 0.2 \) and circles: \( R > 0.4 \).

FIG. 4. The requirement for Eve’s error rate as a function of Bob’s error rate to achieve secure key distribution against opaque attack. Lines are calculated for the values of the Bob’s error rate without eavesdropping.

FIG. 5. Experimental set up for demonstration of the Yuen-Kim protocol. In Alice’s transmitter, pattern generators (PG) drive two lasers. ATT., ATT1 and ATT2 are attenuators. In the receivers of Bob and Eve, the light in one of the divided path is delayed. Lights are detected by balanced detectors made of two photodiodes. ADC: analog-digital converters. PC: personal computer.

FIG. 6. A typical probability distribution of the output signal from the amplifier. Diamonds denote experimental result, broken lines show the Gaussians used for fitting, and the solid line shows the sum of those two Gaussians.
Fig. 1 of “Security of classical noise-based cryptography” by Tomita and Hirota
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Fig. 4 of “Security of classical noise-based cryptography” by Tomita and Hirota
Fig. 5 of “Security of classical noise-based cryptography” by Tomita and Hirota
Fig. 6 of “Security of classical noise-based cryptography” by Tomita and Hirota