Achieving Economic Operation and Secondary Frequency Regulation Simultaneously Through Feedback Control

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Abstract—This article presents an exciting finding for the power industry: the parameters of secondary frequency control based on integral or proportional integral control can be tuned to achieve economic operation and frequency regulation simultaneously. We show that if the power imbalance is represented by frequency deviation, an iterative dual decomposition based economic dispatch solving is equivalent to integral control. An iterative method of multipliers based economic dispatch is equivalent to proportional integral control. Similarly, if the controller parameters of the secondary frequency controllers are chosen based on generator cost functions, these secondary frequency controllers achieve both economic operation and frequency regulation simultaneously.

Index Terms—Economic dispatch; dual decomposition; method of multipliers; secondary frequency control

I. INTRODUCTION

We will start with a two-area system to explain our finding. In Section II, dual decomposition based iterative economic dispatch problem is presented. The corresponding continuous dynamic model is then derived. In Section III, method of multipliers based iterative approach is presented. The continuous dynamic model is again derived. We show that if the power imbalance can be represented by frequency deviation, the former approach is similar as integral control and the latter approach is similar as proportional integral control.

This finding has a revolutionary meaning for the power industry. The parameters of the feedback control for each generator (input: frequency deviation, output: turbine-governor’s power reference) can be selected according to generator cost functions. This selection will lead to frequency regulation and economic operation simultaneously.

II. DUAL DECOMPOSITION BASED ITERATIVE ECONOMIC DISPATCH

For a two-area system, each area with a generator (dispatch level \(P_i\)) and a load \((D_i)\), the economic dispatch problem is expressed as follows.

\[
\min_{P_1, P_2} \quad C_1(P_1) + C_2(P_2) \\
\text{subject to:} \quad P_1 + P_2 = D_1 + D_2. \tag{1}
\]

where \(C_i(P_i) = a_i P_i^2 + b_i P_i + C_i\) is the cost function.

The dual problem is as follows.

\[
\max_{\lambda} \min_{P_1} \quad C_1(P_1) + \lambda(D_1 - P_1) \\
+ \min_{P_2} \quad C_2(P_2) + \lambda(D_2 - P_2) \tag{2}
\]

For a given \(\lambda\), Area 1 and Area 2 can carry out minimization problems separately. The price \(\lambda\) is then updated to maximize the objective function of the dual problem. In addition, the power imbalance will be represented by the frequency deviation with a gain. The iterative procedure of \(\lambda\) update is as follows.

\[
\lambda^{k+1} = \lambda^k + \alpha(D_1 + D_2 - P_1 - P_2) \tag{3}
\]

\[
\lambda^k = K \Delta f^k \tag{4}
\]

Ignoring the generator limits, the marginal costs of the generators should equal to the price at each step.

\[
\lambda^k = 2a_1 P_1^k + b_1 = 2a_2 P_2^k + b_2. \tag{5}
\]

Therefore, the iteration for the power commands that will be sent to the turbine governors are:

\[
P_1^{k+1} = P_1^k - \frac{K}{2a_1} \Delta f_1^k \tag{6}
\]

\[
P_2^{k+1} = P_2^k - \frac{K}{2a_2} \Delta f_2^k \tag{7}
\]

The continuous dynamic model of the above procedure can be obtained using Forward Euler approximation for derivatives.

\[
\tau \dot{P}_1 = -\frac{K}{2a_1} \Delta f_1 \tag{8}
\]

\[
\tau \dot{P}_2 = -\frac{K}{2a_2} \Delta f_2 \tag{9}
\]

where \(\tau\) is the step size of the discrete iteration.

Remarks: the continuous dynamic model not only indicates that dual decomposition-based economic dispatch is equivalent to an integrator in secondary frequency control, but also indicates that if the gains of the integral controllers for generators are chosen based on generators’ cost functions, the local feedback control can realize economic dispatch and frequency regulation simultaneously.
III. Method of Multipliers Based Iterative Economic Dispatch

In method of multipliers, an additional term related to an equality constraint is added to the objective function. The advantage of method of multipliers is to achieve faster convergence compared to dual accent method \[1\]. Our economic dispatch problem now becomes:

$$
\min \quad C_1(P_1) + C_2(P_2) + \frac{\rho}{2}(P_1 + P_2 - D_1 - D_2)^2
$$

subject to: \(P_1 + P_2 = D_1 + D_2\).

Again, the power imbalance can be reflected by frequency deviation. The \(\lambda\) update procedure now becomes

$$
\lambda^{k+1} = \lambda^k + \rho(D_1 + D_2 - P_1^k - P_2^k) = \lambda^k - K\Delta f.
$$

For a given \(\lambda^k\), \(P_1^k\) and \(P_2^k\) should minimize the following objective function:

$$
L(P_1, P_2) = C_1(P_1) + C_2(P_2) + \frac{\rho}{2}(P_1 + P_2 - D_1 - D_2)^2 + \lambda^k(D_1 + D_2 - P_1 - P_2).
$$

The arguments that minimize \(L(P_1, P_2)\) can be found by setting the gradients related to \(P_1\) and \(P_2\) to zeros.

$$
\frac{\partial L}{\partial P_1} = 0, \quad \frac{\partial L}{\partial P_2} = 0.
$$

For the two-area system, we find the relationship of \(P_1^k, P_2^k\) versus \(\lambda^k\) as follows.

$$
\lambda^k = 2a_1P_1^k + b_1 - \rho(D_1 + D_2 - P_1^k - P_2^k),
$$

$$
P_1^k = 2a_2P_2^k + b_2 - \rho(D_1 + D_2 - P_1^k - P_2^k).
$$

The iteration for the power commands can be found by replacing \(\lambda\) in (12) by (13).

$$
2a_1(P_1^{k+1} - P_1^k) + K(\Delta f^{k+1} - \Delta f^k) = -K\Delta f^k
$$

$$
2a_2(P_2^{k+1} - P_2^k) + K(\Delta f^{k+1} - \Delta f^k) = -K\Delta f^k.
$$

Using the Forward Euler approximation for derivatives, the continuous dynamic model is the found to be:

$$
2a_1\tau \dot{P}_1 + K\tau \dot{f} = -K\dot{f}_1
$$

$$
2a_2\tau \dot{P}_2 + K\tau \dot{f} = -K\dot{f}_2.
$$

The transfer functions for the above model are as follows.

$$
P_1 = \frac{-K}{2a_1} \left(1 + \frac{1}{\tau s}\right)
$$

$$
P_2 = \frac{-K}{2a_2} \left(1 + \frac{1}{\tau s}\right).
$$

Remarks: The continuous dynamic model not only indicates that method of multipliers-based economic dispatch is equivalent to a proportional integral (PI) controller in secondary frequency control, but also indicates that if the gains of the PI controllers for generators are chosen based on generators’ cost functions, the local feedback control can realize economic dispatch and frequency regulation simultaneously.

The two dynamic models also indicate that method of multiplier-based iteration can achieve faster convergence compared to dual decomposition-based iteration. The former is viewed as a PI control while the latter is viewed as an integral controller. The PI controller should lead to faster response than the integral controller.

IV. Conclusion

In this article, we claimed findings of important practice value for the power industry. The finding is regarding secondary frequency control: the parameters of the controls can be set based on generators’ cost functions to realize economic operation. We discovered the findings by examining the approximate continuous models for two iterative approaches: method of multipliers and dual decomposition. The former is equivalent to PI control while the latter is equivalent to integral control.

References

[1] S. Boyd, N. Parikh, E. Chu, B. Peleato, and J. Eckstein, “Distributed optimization and statistical learning via the alternating direction method of multipliers,” Foundations and Trends® in Machine Learning, vol. 3, no. 1, pp. 1–122, 2011.

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