Fractal Analysis of BOLD Time Series in a Network Associated With Waiting Impulsivity

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Fractal phenomena can be found in numerous scientific areas including neuroscience. Fractals are structures, in which the whole has the same shape as its parts. A specific structure known as pink noise (also called fractal or 1/f noise) is one key fractal manifestation, exhibits both stability and adaptability, and can be addressed via the Hurst exponent (H). FMRI studies using H on regional fMRI time courses used fractality as an important characteristic to unravel neural networks from artificial noise. In this fMRI-study, we examined 103 healthy male students at rest and while performing the 5-choice serial reaction time task. We addressed fractality in a network associated with waiting impulsivity using the adaptive fractal analysis (AFA) approach to determine H. We revealed the fractal nature of the impulsivity network. Furthermore, fractality was influenced by individual impulsivity in terms of decreasing fractality with higher impulsivity in regions of top-down control (left middle frontal gyrus) as well as reward processing (nucleus accumbens and anterior cingulate cortex). We conclude that fractality as determined via H is a promising marker to quantify deviations in network functions at an early stage and, thus, to be able to inform preventive interventions before the manifestation of a disorder.

Keywords: fMRI, Hurst Exponent, frontal cortex, nucleus accumbens, biomarker, impulse control disorders

INTRODUCTION

Fractal structures possess the property that the whole structure consists of parts, which have the same pattern composition but at different scales and/or in different sizes [e.g., broccoli, the Koch snowflake (Koch, 1904, 1906; Mandelbrot, 1967, 1983)]. Fractals can be found not only in static objects but also dynamic processes. This property of self-similarity, or in the temporal domain scale invariance (Suckling et al., 2008; Ivanov et al., 2009; Nagy et al., 2017) means that both, rapidly occurring changes and slowly proceeding dynamics follow the same structure, or better, that measures of the patterns are independent of the sampling rate, used during data acquisition (Riley et al., 2012).
For time series, this property is mathematically expressed as follows:

\[ S(f) = \frac{C_f}{|f|^{\beta}} \]  

\[ \beta = 2H - 1 \]  

\( S(f) \) represents the power spectrum density of the analyzed fluctuations, \( f \) the frequency, \( C_f \) a constant and \( 0 < \beta < 2 \). Furthermore, \( \beta \) is related to the Hurst Exponent (\( H \)) according to Equation 2 (see Figure 1). For more details on how to compute \( H \) refer to method section fractal analysis (AFA) as suggested by Riley et al. (2012).

Fractal patterns have been examined in many research fields including physiology and neuroscience. A specific phenomenon called pink noise (also called fractal or \( 1/f \) noise, with \( \beta = 1 \)) is one of the key fractal manifestations. Pink noise is a stochastic process, used for the modeling of dynamic systems. Its power spectral density is inversely proportional to the sample frequency (Keshner, 1982; Eke et al., 2000, 2002). Because pink or \( 1/f \) noise lies between white noise (\( \frac{1}{f^0} \) or random noise), and red/Brownian noise (\( \frac{1}{f^2} \), power density decreases with increasing frequency), it has been proven to bring stability and adaptability into dynamic processes, thus, crucial properties of well-functioning complex systems (Bak et al., 1987). Pink noise has been documented in behavioral as well as physiological processes, for example in heartbeat dynamics (Ivanov et al., 1999, 2001), neural network organization (Lipsitz and Goldberger, 1992; Lipsitz, 2002) and cognitive processes (Ihlen and Vereijken, 2010; Wijnants et al., 2012). The manifold appearance of pink noise has led to the speculation, that “there exists some profound law of nature that applies to all non-equilibrium systems and results in such noise” (Sejdić and Lipsitz, 2013). Intuitively, one might assume that pink noise has a detrimental effect to a system’s performance and accuracy. However, as pink noise arises from the interaction of multiple systems and operates over different scales, it has been shown to contribute to system resiliency and structural integrity if individual components were lost or interrupted for example by age or disease (Lipsitz and Goldberger, 1992; Lipsitz, 2002). Thus, a fractal network structure, thus, qualifies a system to cope with stress or disturbances by adjusting specific components and fine tuning its responses (for a review see Sejdić and Lipsitz, 2013).

Pink noise can be found in the fMRI signal (i.e., the Blood-Oxygen-Level-Dependent, BOLD response) (Bullmore et al., 2009; He, 2011; Herman et al., 2011; Ciuciu et al., 2012, 2014; Eke et al., 2012; Churchill et al., 2016; Nagy et al., 2017). \( H \) valued close to 1 in the fMRI signal has been associated with a higher predictability of time series (Gentili et al., 2017), greater low-frequency power and, therefore, higher persistence over time (Ball et al., 2011), as well as highly complex and well attuned dynamics in the underlying network (Lipsitz and Goldberger, 1992; Goldberger et al., 2002). Likewise, it has been shown that deviation from pink noise in relevant parameters, independent of whether the changes occurred in the direction of white or red noise, was associated with neurological as well as psychiatric disorders (resting-state fMRI in Alzheimer’s disease: Maxim et al., 2005; e.g., reaction time sequences in attention deficit/hyperactivity disorder: Gilden and Hancock, 2007).

In addition, fractality seem to be more pronounced in low compared to high frequencies. For example, Fox et al. (2007) reported \( 1/f \) noise in the fMRI signal (Fox et al., 2007), emphasizing that “spontaneous BOLD follow a \( 1/f \) distribution, meaning that there is an increasing power in the low frequencies.” (Fox and Raichle, 2007). In addition, Gentili et al. (2017) found brain regions where \( H \) as well as metrics of low-frequency oscillations (i.e., amplitude of low-frequency fluctuations, ALFF; fractional amplitude of low-frequency fluctuations, fALFF) had similar effects hinting toward strong relation between both measures (Gentili et al., 2017). In task-fMRI data, fractal noise of inactive voxels differed from those of active ones (Thurner et al., 2003). Recent resting-state fMRI-studies showed, that \( H \) correlated with personality traits such as anxiety (Gentili et al., 2015) and extraversion (Gentili et al., 2017) in regions of the default mode network, with response time in the inferior frontal gyrus (Wink et al., 2008) hinting toward an influence of personality traits and task performance on the persistence of network dynamics (Wink et al., 2008). Likewise, findings from task-fMRI studies reported that \( H \) decreased with task processing (Ciuciu et al., 2012) and cognitive effort (Barnes et al., 2009; Churchill et al., 2016) concluding that “task-related modulation of multifractality appears only significant in functional networks and thus can be considered as the key property disentangling functional networks from artifacts” (Ciuciu et al., 2012).

Impulsivity is a personality trait, which spans from normal manifestations, e.g., in life time situations where decision making under time pressure is required (Burnett Heyes et al., 2012), to pathological presentations, mirroring the psychiatric symptoms of “loss of control” and “impulse control disorder” associated for example with ADHD (e.g., Sebastian et al., 2013; for a recent review see Hinshaw, 2017). Waiting impulsivity (WI) is one form of impulsivity and is operationally defined as the tendency to premature responding, i.e., to respond before target onset. Thus, it involves the aspects of response inhibition and top-down control, mediated by motivational aspects and reward processing (Robinson et al., 2009; Voon et al., 2014). Its associated functional network consists of the dlPFC and the vmPFC representing impulse control (Mechelans et al., 2017), the reward-perception-related NAcc, the ACC for the cognitive evaluation of the reward and hippocampus (HC) and amygdala (AMY) responsible for reward-based learning (Dalley et al., 2011). Impulsivity has been documented to affect on the behavioral performance of attentional functions, working memory, motor speed, and language processing (Hinshaw et al.,...
In brain activation, high impulsive healthy subjects showed reduced activation in right dorsolateral prefrontal cortex (dPFC) while performing a decision making task (Deserno et al., 2015), bilaterally in the ventral prefrontal cortex (vmPFC) during motor inhibition (Goya-Maldonado et al., 2010) as well as in the dPFC and the hippocampus in aggressive impulsive subjects (Sala et al., 2011). At rest, impulsivity affected functional connectivity from resting-state fMRI in terms of less elaborated neural network architecture, e.g., lateral and medial prefrontal regions were isolated from reward associated regions such as the nucleus accumbens (NAcc) (Davis et al., 2013), connectivity between the NAcc and the anterior cingulate cortex (ACC) as well as the ACC and the amygdala (Li et al., 2013). A first study addressing the influence of impulsivity on H revealed that impulsivity correlated negatively with H in the orbitofrontal cortex (i.e., the vmPFC) and NAcc (Hahn et al., 2012) the way that the higher impulsive the subjects the smaller the H.

In this study, we examined the fractal nature of a brain network associated with WI using the AFA approach. H was determined for all network regions at rest and while performing a WI task. To define, whether a subject is high (highImp) or low impulsive (lowImp), the number of premature responses has been used (Feja et al., 2014; e.g., Donnelly et al., 2014). A permutation test was performed to insure the validity of using the number of premature responses as grouping criteria (see Supplementary permutation.xlsx—Supplementary Datasheet 1).

Based on the introduced findings we were intrigued to address the existence of pink noise in our network, thus, we expected to find

(a) a fractal nature of the impulsivity network and that fractality consists of pink noise, i.e., H values of all network regions were close to 1.

(b) smaller H at task compared to rest (Barnes et al., 2009; Ciuciu et al., 2012; Churchill et al., 2016).

(c) significant influence of impulsivity on H predominantly in the PFC and the NAcc (Wink et al., 2008; Hahn et al., 2012).

In line with the previous studies (Gilden and Hancock, 2007; Hausdorff, 2007) we expected to find deviation from 1/f noise pronounced in highImp compared to lowImp subjects.

**MATERIALS AND METHODS**

**Subjects**

In this study, data of the same sample of 103 students was used as described by Neufang et al. (2016). Students were between 19 and 28 years old (24.0 ± 2.6 years), and were recruited at the University of Wuerzburg, Germany. From all subjects, measures for impulsivity were collected, using the Wender-Reimherr-Interview and Attention-Deficit/Hyperactivity Disorder checklist (subscales “impulsivity” and “hyperactivity and impulse control”) (Rösler et al., 2008). The examination was conducted in accordance with the Declaration of Helsinki in its latest version from 2008 and was approved by the ethics committee of the Faculty of Medicine, University of Wuerzburg, and written informed consent was obtained from all subjects.

**Experimental Paradigm**

The used paradigm was an fMRI-adaptation of the four-choice serial reaction time task by Voon et al. (2014) and has been described in detail by Neufang et al. (2016), Voon et al. (2014), and Neufang et al. (2016). The task entailed the detection of a brief visual target (a green dot) after a certain waiting period. Depending on the subject's task performance, a reward of 1 Euro or 1 Cent was given, or better the punishment of 1 Euro was subtracted. In detail, a trial implied three phases/experimental conditions: the “cue” presentation, indicating the start of the waiting period; the “target” onset, in terms of a green circle in one of the choices. Subjects were instructed to indicate the correct choice by pressing the corresponding button as fast and as correct as possible; the reward feedback, showing the amount of recently earned/lost money in combination with the overall amount of earned money (see Figure 2).

The task consisted of one baseline run outside the scanner and five experimental runs within the scanner. During the five runs in the scanner, WI was experimentally manipulated by (i) implementing a monetary reward (blobs 1, 3, 4, 5), (ii) varying the duration of the target presentation (blobs 3, 4, 5), (c) extending the waiting period (cue-target interval) (blobs 4 and 5) and (d) presenting additional distractor taget before the actual target presentation, i.e., circles in different colors (block 5). Task scanning was of a total duration of 14 min.

![Figure 1](https://example.com/figure1.png)

**FIGURE 1** | The 1/f noise pattern in a power spectrum (Equation 1) of an exemplary time course is shown on logarithmic scales while the scale invariance relation (Equation 3) is indicated by the slope H. Please note, that the relationship between β and H is according to Equation (2) $\beta = 2H - 1$. For demonstration, the example of a representative individual time course of the right MFG during task has been used.
Before task-fMRI, all subjects were scanned at rest for 12 min. During the rs-fMRI, subjects kept their eyes open and were instructed not to think of something specific. Eyes were controlled by the examiner via an eye tracking camera outside the MR scanner.

**fMRI—Data Acquisition**

The fMRI scanner was a 3 Tesla TIM Trio Scanner (Siemens, Erlangen, Germany). Functional MRI included a T2*-weighted gradient echo-planar imaging sequence with the following sequence parameters: repetition time (TR) = 2000 ms, echo time (TE) = 30 ms, 36 slices, 3 mm thickness, field of view (FoV) = 192 mm, flip angle = 90°, number of volumes in task-fMRI = 425, number of volumes in rs-fMRI = 350).

**fMRI—Data Processing**

Data preprocessing was performed using the Statistical Parametric Mapping Software Package (SPM12). Preprocessing followed the standard routine including temporal and spatial alignment, i.e., slice time correction and realignment and unwarp, spatial normalization [standard space: Montreal Neurological Institute (MNI) space] including a resampling of the data to an isotropic voxel size of \(2 \times 2 \times 2\) mm\(^3\), spatial smoothing with a Gaussian kernel of 8 mm full width at half maximum (FWHM), and linear trend removal [using the matlab routine detrend (y)] (see Supplementary Presentation 1) (Bai et al., 2008; Zhang et al., 2008; Fox et al., 2009; Qiu et al., 2011). Pre-processing did not include high-pass filtering or global mean correction.

**fMRI Time Course Extraction**

Regions of Interest (ROI) were defined based on the significantly activated brain regions while performing the waiting impulsivity task. In detail, for the identification of global activation maxima, the contrasts target > baseline and reward > baseline were defined on a single subject level and analyzed on group level using a one sample t-test. The local maxima of each significantly activated regions were identified and coordinates were then used as the centre of a 10 mm spheric ROI using MarsBar [24]. ROIs were built and used for the extraction of the time course for each subject. Time course extraction was performed using the routine as suggested by Brett et al. (2002) (see MarsBar manual, http://marsbar.sourceforge.net/marsbar.pdf) from preprocessed fMRI data (i.e., smoothed files resulting from the pre-processing procedure) (Brett et al., 2002).

**AFA**

Fractal analysis of time series is based on quantifying the degree of fluctuation around the overall trend of the data over time, to measure the scale invariance quantified by the value of \(H\) (Equation 3, see below). In this paper, we split the fMRI signal in its two components: the low and the high frequency components (LFC, HFC) (see Figure 3).

LFC is the second order polynomial that is a smooth and global fit of the original time course (see Figure 4). HFC represents the residuals after subtracting the fitting curve from the original time course. For time series to be fractal, their power spectrum density (PSD) must be inversely proportional to frequency (see also Figure 5, legend).

After analyzing these two main components, we found, that the residuals were more likely to obscure the results with respect to the scale invariance analysis. HFC, in addition, could not be classified as fractal (see Figure 5A). The low frequency component of the signal on the other hand, held all the information concerning the fractal nature of the original signal. In line with earlier studies and to avoid inaccuracies and the reduction of \(H\), we focused in our analyses on those parts of the signal/those regions, which showed power law scaling and fractal scaling was present (e.g., Cannon et al., 1997; Herman et al., 2011; Riley et al., 2012): only the LCF was taken into consideration for further analysis via AFA to compute \(H\).

AFA is one of the existing mathematical methods that computes \(H\), a factor that reflects in a scale law manner the relationship, that is intrinsic to fractal processes, between the variance of fluctuation computed around, in our case, a second order polynomial trend \(v(i)\) fitted to time series within each segment \(w\), and its size:

\[
F(w) = \left(\frac{1}{N} \sum_{i=1}^{N} (u(i) - v(i))^2\right)^{\frac{1}{2}} \sim w^H, \tag{3}
\]

\(N\): length of the time series
\(w = 2n + 1, n = 5, 6 \ldots, 13\)

\(H\) is determined as the slope of the log-log diffusion plot \(\log_2(F(w))\) as a function of \(\log_2(w)\) (see Figure 1B).

**Statistical Analysis**

The factor impulsive phenotype was defined as high impulsive (highImp) versus low impulsive subjects (lowImp), based on the subjects’ number of premature responses. If the number was \(\geq 3\) they were classified as highImp and if the number was \(<3\) as lowImp. Threshold definition was adapted from Feja et al. (2014) in terms of the median value of premature responses across all subjects [range: 0–6 number of premature responses]
FIGURE 3 | Power frequency spectrum of the original time course (black dots), as well as of the resulting low (yellow line) and high frequency (red line) components. Please note the overlap between the black dots (original time course) and the yellow line (LFC) in low frequencies (left part of the x-axis) and between the black dots and the red line (HFC) in high frequencies (right part of the x-axis). The same time course of the right MFG during task of a representative subject has been used.

FIGURE 4 | Overlap between low frequency course (LFC) and the original time course. LFC fits well the data without overfitting leaving out unnecessary information for the fractal analysis. In this figure, the same time course of the right MFG during task of a representative subject has been used.

(adapted from Feja et al., 2014). The sample consisted of 66 lowImp subjects and 38 highImp. In addition, a permutation test was performed to insure the validity of using the number of premature responses as grouping criteria (see Supplement permutation.xlsx—Supplementary Datasheet 1).

On behavioral level, $1 \times 2$ ANOVA models were defined using the between-subject factor impulsivity phenotype (highImp vs. lowImp) as independent factor and the dependent variables the behavioral parameters no. of premature responses, accuracy, reward (amount of total win) and reaction times.

The question of the existence of pink noise was verified using a one sample Wilcoxon test with $H$ of all network regions as test variables and 1 as hypothetical median.

To address the two aspects (a) changes in fractality at rest and while task processing and (b) the influence of impulsivity on fractality of the impulsivity network, the following statistical analyses were performed:

(a) To compare fractality at rest and while task processing, non-parametric tests of related samples were defined using the within-subject factor condition (task vs. rest), and $H$ as dependent variable. To reveal the impact of the impulsive phenotype on differences between rest and task, the same analyses were performed phenotype-specifically.

(b) The influence of impulsivity on network fractality was performed using both, the factorial and the dimensional
approach. Impulsive phenotype differences of \( H \) were addressed using non-parametric Mann-Whitney-U-Test for 2 independent samples using the between-subject factor *impulsive phenotype* and dependent variables were \( H \) scores. In addition, correlations between WI (i.e., the number of premature responses, task accuracy, reward and reaction times) and \( H \) scores were performed.

For all statistical analyses a significance threshold of \( p < 0.05 \), corrected for multiple comparisons using the False-Discovery Rate (Benjamini and Hochberg, 1995), was applied. The number of test as well as \( q^* \)-scores representing the FDR-corrected significance levels were provided for each analysis in the results section as well as in Tables 1, 2.

**RESULTS**

*post-hoc* power analyses using G*Power* (version 3.1.9.3, [http://www.gpower.hhu.de/](http://www.gpower.hhu.de/)) revealed a power of 0.77 and a critical \( Z = 1.6 \).

Regarding behavioral differences only main effect of impulsive phenotype on the number of premature responses passed the threshold of significance (\( M_{\text{lowImp}} = 0.6 \pm 0.5 \), \( M_{\text{highImp}} = 2.5 \pm 0.9 \), \( F_{(102, 2)} = 201.8 \), \( p = 0.000 \), corrected for 4 comparisons with \( q^* = 0.0125 \)). All other effects on any other dependent variable were not significant (for further results please see Neufang et al., 2016).

Performed fMRI analyses revealed that whereas activation bilaterally in the middle frontal gyrus (MFG) (right MFG: \( x = 40 \), \( y = 0.8 \), \( z = 34 \), \( T = 19.7 \); left MFG: \( x = -44 \), \( y = 6 \), \( z = 28 \), \( T = 21.7 \)), the ACC (\( x = 6 \), \( y = 30 \), \( z = 28 \), \( T = 18.6 \)) as well as the vmPFC (\( x = 0 \), \( y = 48 \), \( z = -12 \), \( T = 6.5 \)) was associated with impulse control, bilaterally the HC (right HC: \( x = 24 \), \( y = -28 \), \( z = -6 \), \( T = 21.9 \); left HC: \( x = -22 \), \( y = -28 \), \( z = -6 \), \( T = 17.7 \)), the right NAcc (\( x = 8 \), \( y = 12 \), \( z = -10 \), \( T = 14.6 \)), and the left amygdala (\( x = -22 \), \( y = 0 \), \( z = -12 \), \( T = 6.0 \)) were active while reward processing (see Figure 6).

Via AFA we found that at rest (a) across all subjects, \( H \) was similar to 1 in the following network regions (HC: \( M = 0.93 \pm 0.13 \), \( p = 0.000 \); ACC: \( M = 0.96 \pm 0.12 \), \( p = 0.000 \); lMFG: \( M = 1.01 \pm 0.12 \), \( p = 0.156 \); rMFG: \( M = 1.00 \pm 0.12 \), \( p = 0.577 \); ACC: \( M = 1.01 \pm 0.12 \), \( p = 0.414 \); rNAcc: \( M = 1.03 \pm 0.10 \), \( p = 0.060 \); lAMY: \( M = 1.00 \pm 0.11 \), \( p = 0.928 \); vmPFC: \( M = 1.01 \pm 0.12 \), \( p = 0.087 \), corrected for 8 comparisons with \( q^* = 0.060 \)) proving a stable fractal nature of this network for confidence intervals from bootstrap see Supplementary Table 1.

(a) Across all subjects (i.e., independent of the impulsive phenotype), \( H \) was significantly higher at rest compared to task in all regions. Group-specific analyses, however, revealed that in highImp subjects, fractality in the right HC did not differ at rest and during task processing (see Table 1). In lowImp subjects, \( H \) was significantly higher at rest compared to task in all regions.

(b) \( H \) during task-processing differed between impulsivity phenotypes in terms of reduced \( H \) in highImp subjects in the reward-associated NAcc and the impulse control-related ACC (see Table 2). Furthermore, \( H \) of the left HC varied trend-wise between impulsivity groups across. At rest, there was no significant difference in any region. Correlations revealed a significant correlation between \( H \) of the left MFG and the number of premature responses (\( r = -0.242 \), \( p = 0.013 \), corrected for 16 comparisons with \( q^* = 0.012 \)), whereas there was no significant relation between \( H \) and accuracy, reward and reaction times.

**DISCUSSION**

In this study, we addressed the fractal nature of a neural network associated with waiting impulsivity. We found that (a) pink noise in all network regions, proving the existence of a stable fractal nature within this network (Bak et al., 1987; Lipsitz and Goldberger, 1992; Lipsitz, 2002; Wijnants et al., 2012). Furthermore, (b) \( H \) was significantly higher at rest compared to task. This was the case in all regions and across all subjects. However, in high impulsive (highImp) subjects, \( H \) was comparable between both activation conditions in the right HC. (c) Finally, during task processing, fractality in impulse control related left MFG as well as reward-associated NAcc and ACC was influenced by impulsivity the way that in highImp subjects \( H \) was significantly smaller and, therefore, was a less adequate 1/f noise fit candidate compared to lowImp subjects.
The Fractal Nature of the Waiting Impulsivity Network

As introduced we learned that a brain network follows a stable fractal patterns when H is close to 1 (e.g., Stadnitski, 2012), is decreased while cognitive activation (Barnes et al., 2009; Ciuciu et al., 2012; Churchill et al., 2016), and is sensitive to normal and abnormal alteration such as disease or age (Lipsitz and Goldberger, 1992; Lipsitz, 2002; Sejdić and Lipsitz, 2013). In our data, we could find all these aspects and, hence, assumed a fractal nature in the impulsivity network: (a) at rest, H varied around 1 across all subjects; during task processing, H was significantly reduced in all regions and, finally, when comparing H between high and low impulsive subjects, H was reduced in highImp subjects in some of the network regions. The network examined here has been introduced in a comprehensive review article by Dalley et al. (2011) and is based on relevant findings from humans and animal studies on impulsivity and cognitive top-down control (Dalley et al., 2011). The notion that the suggested network regions were indeed involved in the processes of waiting impulsivity as measured via the 5-CSRTT has been shown in recent studies (NAcc and ACC: Morris et al., 2016; e.g., NAcc and vmPFC: Neufang et al., 2016; dIPFC and ACC: Mechelmanns et al., 2017). The characterization of this network as a "healthy and complex system" (Bak et al., 1987), however, has been demonstrated in this study for the first time.

Fractality During Task Processing and at Rest

Higher fractality at rest compared to task processing/cognitive effort is in line with earlier findings (He, 2011; Ciuciu et al., 2012; Churchill et al., 2016). In the context of the common knowledge, that neural networks are predominantly active after an external stimulation, e.g., of our senses or while cognitive processing (Penn and Shatz, 1999; Kandel et al., 2000), this finding seems counter-intuitive. However, the recent years of research on the brain at rest have accentuated the prominence of endogenously engendered brain responses as an important defining factor in modeling the topology of large-scale neuronal networks (for reviews see Linkenkaer-Hansen, 2002; Calhoun and De Lacy, 2017; Gorges et al., 2017; Liégeois et al., 2017; Smitha et al., 2017). The terms used most frequently to describe resting-state neural activity, such as “endogenous,” “intrinsic” and “spontaneous,” indicate that network function is created within the brain itself, and can, thus, be understood as “self-organized” (Linkenkaer-Hansen, 2002). Self-organized criticality, in return, has been described by Bak et al. (1987) as the origin of fractal objects. They demonstrated, that “dynamic systems naturally evolve into self-organized critical structures of states” and suggested, that “this self-organized criticality is the common underlying mechanism” behind those dynamic system (Bak et al., 1987). For an empirical example in the context of sleep dynamics, Lo et al. (2013) were able to identify two independent paths for the transition between sleep phases using power-law scaling on nocturnal EEG recordings (Lo et al., 2013). Thus, a task-induced stimulation operating as an involvement from the outside system may lead to a reduction of these dynamics, hence of fractality.
In highImp subjects, however, $H$ did not decrease significantly during task in the right HC. A generally small fractality in the hippocampus has been reported by He (2011, 2014). They found varying $H$ across different cortical regions with lowest $H$ in the HC, interpreting these findings in terms of regional differences in neurovascular coupling mechanisms (He, 2011, 2014). Impaired hippocampal $H$ has also been reported between patients with Alzheimer’s disease and control subjects (Maxim et al., 2005) with the persistence of $H$ being assumed to reflect neurodegenerative processes. The insignificant change of $H$ during task processing in high impulsive subjects in our study, thus, might reflect a weaker recruitment of the right HC while performing the task and a more superficial learning (e.g., El-Gaby et al., 2015). In return, this finding can also be interpreted the way, that the right HC is less adaptive in high impulsive subjects, thus constantly following its own dynamics, leading to an impaired motivation- or reward-based learning of the task (Chantiluke et al., 2012; Moreno-López et al., 2012).

**Fractality Differs in Function of Impulsivity**

Our analyses revealed, that impulsivity modulated fractality only during task processing and predominantly in the fronto-striatal loop namely the ACC and the NAcc, as well as the left MFG. Morris et al. (2016) showed that functional connectivity in the ACC and the NAcc via the subthalamic nucleus varied in function of the number of premature responses (Morris et al., 2016) emphasizing the crucial and interacting role of these two structures on the key parameter of waiting impulsivity. The left MFG as part of the dorsolateral PFC, in return, reflects the counterpart, i.e., top-down control which decreases with higher reward processing (Mechelmans et al., 2017).

In the NAcc as well as in the ACC, in high impulsive subjects, $H$ was significantly reduced compared to low impulsive subjects. A negative association between impulsivity/reward sensitivity and the ventral striatum has been reported by Hahn et al. (2012) before in the way that the higher impulsive/reward sensitive the subjects were, the smaller the $H$ (Hahn et al., 2012). Reduced $H$ in the NAcc and ACC in high impulsive subjects of our study, thus, reflects an altered reward processing.

In addition, significant correlations between impulsivity and fractality in the frontal cortex have been shown for the orbitofrontal cortex (Hahn et al., 2012) as well as for the lateral PFC (Ball et al., 2011). Similar to these findings, we found a significant (negative) correlation with the number of premature responses and $H$ in the left MFG across all subjects as well as in the vmPFC in the highImp group. The MFG is strongly involved in response inhibition and cognitive control (Chambers et al., 2009; Boehler et al., 2010; Braver, 2012; Bari and Robbins, 2013), thus, a more random top-down control in highImp subjects reflects impaired control and more impulsive task performance. Taken together, the combination of impaired top-down control and altered reward processing is common and has been described for numerous impulse control disorders.
such as attention-deficit/hyperactivity disorder (e.g., Scheres and Hamaker, 2010), eating disorders (for review Citrome, 2015), addiction (Weinstein, 2017), bipolar disorder, and depression (Carver et al., 2008).

In contrast to findings by Wink et al., H of network regions associated with waiting impulsivity did not correlate with reaction time (Wink et al., 2008). This, however, might be based on the different anatomical structures: Wink et al. reported a correlation of H and resting-state fMRI signals in the right inferior frontal cortex, which was not included in our network.

LIMITATION AND CONCLUSION

In this study, we chose a monofractal approach. The main reasons were the following: (1) This is a pilot study for a clinical project; thus, data acquisition was strongly determined by the factors (a) field strength (3T) (b) total scanning time (12 min/365 volumes during resting-state; 14 min/420 volumes during task), (c) sample rate (TR was 2000 ms) to ensure the feasibility for patients to perform the scanning procedure successfully. All factors, however, play a crucial role in the analysis of fractal patterns in fMRI (Eke et al., 2012). For example, the field strength highly influences measurement sensitivity (Eke et al., 2006) and multi-fractal analysis is “known to require a much higher signal definition for an optimal performance” than monofractal (Ciuciu et al., 2012; Eke et al., 2012). Likewise, multi-fractal analyses need longer time series/higher sampling rates than those found for monofractal series (Eke et al., 2002, 2012). (2) In a previous step multi-fractality was addressed (using q from −2 to 2) and revealed, that our signals are, with no loss of information, to be approximated as monofractal (see Figure S1). The monofractal approximation, however, has been proven to be a robust assumption and, thus, an adequate tool to address similar signals.

In summary, we revealed that activity in the neural network associated with waiting impulsivity is of fractal nature. The use of fractal parameters to examine neural networks regarding to health or disorder has been described in earlier studies (e.g., Lipsitz, 2002; Maxim et al., 2005; Hahn et al., 2012; Lei et al., 2013; Sokunbi et al., 2014; El-Gaby et al., 2015; Dona et al., 2017; Gorges et al., 2017), introducing these parameters as exceptionally sensitive toward alterations. In our study, however, we performed analysis in a very homogenous sample of young adult male students. The classification into high and low impulsive subjects, therefore, is relative and does not represent samples with manifest impulse control disorders. The transfer of the present data to a clinical context therefore predominantly relies on the findings of earlier studies (e.g., Lipsitz, 2002; Maxim et al., 2005; Hahn et al., 2012; Lei et al., 2013; Sokunbi et al., 2014; El-Gaby et al., 2015; Dona et al., 2017; Gorges et al., 2017) and would be of high interest for future studies.

In contrast to earlier studies, in which H was determined on the whole brain level and in a data-driven manner (e.g., Suckling et al., 2008; Wink et al., 2008; Barnes et al., 2009; Gentili et al., 2015, 2017; Churchill et al., 2016), we chose to focus on an earlier described network. This way, we were able to a priori match cognition and neural structures, however, taking the risk of losing information, for example regarding the compensatory recruitment of additional structures. When examining a clinical sample, thus, a combined approach would be indicated.

Taken together, we would like to emphasize, that the use of fractality and H in particular, has two advantages which makes it a promising biomarker in the early detection of disease: (i) the reference score is a concrete number (e.g., 1) the difference can be interpreted as a measure of the deviation from this reference state, (ii) in principle the assessment of H can be integrated in the (f)MRI clinical routine protocol subject to the availability of sufficiently long fMRI-BOLD sequences. However, consistent with earlier observations with various fractal time series methods (Eke et al., 2000) -, as specifically stated by Riley et al. (2012), “AFA requires careful consideration of signal properties, parameter settings, and interpretation of results, and should not be applied blindly to unfamiliar signals.” (Riley et al., 2012). In line with earlier studies, our data showed the potential of fractal parameters in the detection of altered brain function in the clinical context. For that reason, it is highly recommended to follow up on the development of methods to making fractal analysis accessible to a wider public and delivering unambiguous results.

AUTHOR CONTRIBUTIONS

SN, MR, and AS-B conceptualized and supervised the study, SN and AA acquired and analyzed the data. AS-B, MR, and KD supported the transfer of the findings into the current discussion of translational (AS-B) and clinical neuroscience (MR, KD). All authors contributed to and have approved the final manuscript.

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SUPPLEMENTARY MATERIAL

The Supplementary Material for this article can be found online at: https://www.frontiersin.org/articles/10.3389/fphys.2018.01378/full#supplementary-material

Figure S1 | The scaling function f and the corresponding regression line of the entire signal (left upper row) and for its LFC only (right upper row). Please note that data points in the case of the LFC are linearly fitted, whereas this is not the case in the entire signal. The diagramm in the lower row shows that the slopes H of the regression lines are q-independent (monofractal). For this diagramm, MFDFA has been used (Ihlen, 2012). For demonstration, the example of a representative individual time course has been used.

Supplementary Presentation 1 | Plots of raw BOLD series.
Supplementary Table 1 | Bootstrap.
Supplementary Datasheet 1 | Permutations.
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