Crisscross Harris Hawks Optimizer for Global Tasks and Feature Selection

Xin Wang1 · Xiaogang Dong1 · Yanan Zhang2,3 · Huiling Chen4

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Abstract
Harris Hawks Optimizer (HHO) is a recent well-established optimizer based on the hunting characteristics of Harris hawks, which shows excellent efficiency in solving a variety of optimization issues. However, it undergoes weak global search capability because of the levy distribution in its optimization process. In this paper, a variant of HHO is proposed using Crisscross Optimization Algorithm (CSO) to compensate for the shortcomings of original HHO. The novel developed optimizer called Crisscross Harris Hawks Optimizer (CCHHO), which can effectively achieve high-quality solutions with accelerated convergence on a variety of optimization tasks. In the proposed algorithm, the vertical crossover strategy of CSO is used for adjusting the exploitative ability adaptively to alleviate the local optimum; the horizontal crossover strategy of CSO is considered as an operator for boosting explorative trend; and the competitive operator is adopted to accelerate the convergence rate. The effectiveness of the proposed optimizer is evaluated using 4 kinds of benchmark functions, 3 constrained engineering optimization issues and feature selection problems on 13 datasets from the UCI repository. Comparing with nine conventional intelligence algorithms and 9 state-of-the-art algorithms, the statistical results reveal that the proposed CCHHO is significantly more effective than HHO, CSO, CCNMHHO and other competitors, and its advantage is not influenced by the increase of problems’ dimensions. Additionally, experimental results also illustrate that the proposed CCHHO outperforms some existing optimizers in working out engineering design optimization; for feature selection problems, it is superior to other feature selection methods including CCNMHHO in terms of fitness, error rate and length of selected features.

Keywords Harris hawks optimization · Bioinspired algorithm · Global optimization · Engineering optimization · Feature selection

1 Introduction
Optimization is the procedure of determining the optimal solution for a specific issue with a reasonable computational expense. It has received increasing attentions in a variety of scientific fields of research and engineering and is essential to propose splendid optimization algorithms [1–4]. Traditional deterministic optimization approaches cannot mostly feasible in each real-world problem [4]. As becoming more and more sophisticated, the various optimization issues are extensively solved using the promising stochastic bioinspired algorithms [5–9]. This kind of algorithm is unsensitive to the searching magnitude and has strong optimization capability and flexibility of finding high-quality solution efficiently through a brief process, even for high-dimensional difficult problems [4, 10–18]. A great number of well-regarded bioinspired optimizers, such as Differential Evolution (DE) [19], Particle Swarm Optimization (PSO)
HHO is a newly stochastic bioinspired optimization algorithm with promising performance of dealing with continuous problems. It can provide easy implement and outstanding exploitative capability of local search. The algorithm is developed according to the inspiration of cooperative preying behavior of Harris’ hawks and skilled in converging fast and making a suitable balance between intensification and diversification. The hawks’ dynamic chasing patterns, which are resulted from the natural surrounding and time-vary escaping ways of prey, are composed of six phases, two in exploration phase and the remainder in exploitation phase. With the help of the stochastic operations of six phases, HHO can find excellent solutions compared to other well-regarded algorithms such as Genetic Algorithm (GA) [31], Biogeography-Based Optimization (BBO) [31], DE [31], PSO [31], Cuckoo Search algorithm (CS) [32], TLBO [33], BA/BAT [24], FPA [34], FA [35], GWO [21], and MFO [22]. Additionally, it can be superior to other optimizers in constrained engineering optimization tasks. HHO has already attracted many attentions in a variety of application fields soon after its occurrence [4, 36–49]. These superiority and meaningful applications reveal that HHO is a powerful enough optimizer. Notwithstanding, as a stochastic bioinspired algorithm, HHO also may undergo the shortcomings of trapping into local optima and degrading convergence rate when tackling some complex tasks. On one hand, it undergoes weak global search capability because of the levy distribution in its optimization process, which makes it difficult to run away from the local optima. On the other hand, the strong randomness in exploration phase may result in skipping the search spots at the edge of search space. Third, the “No-Free-Lunch” (NFL) theorem indicated that no optimizer can be the best general approach for all kinds of problems. With the motivation of these considerations, this study employs the CrissCross Optimization Algorithm (CSO) strategy as an operator to improve HHO.

CSO [50] is a well-established stochastic algorithm inspired by crossover behaviors based on the principle of the gold mean in Confucian doctrine. As proposed in its original literature, the simple CSO offers fast convergence rate and high-quality solution with preserving the population diversity when solving not only continuous but also complex optimization problems. A dual crossover search behavior in CSO is employed to establish an interacting chain of horizontal crossover operator and vertical crossover operator. As a global optimization operator, horizontal crossover conducts a crossing over arithmetically on two distinct search agents across all their dimensions, which are, respectively, chosen from the subpopulations without repetition. This operation ensures a larger probability of searching in each subspace and diminishes effectively the unreachable search spots. Vertical crossover is to exchange the dimensional information of a single search agent, which can facilitate escaping from the stagnancy in local optima without destroying other dimensions that may be the global optimum. Considering the advantages of CSO, some papers tried to apply this algorithm on handling complex problems [50–57]. In addition, the excellent search capability of the two crossover operators can exactly make up for the deficiencies of HHO mentioned above. Therefore, this study proposes an improved HHO using these two powerful crossover mechanisms in CSO. The proposed optimizer is called CrissCross Harris Hawks Optimizer (CCHHO).

CCHHO contains three phases. After the first initialization phase, the vertical crossover as a regulation mechanism in the second phase interacts with the exploitative behavior of HHO to modify partial search agents for adjusting the exploitative ability adaptively. With the help of dimensional mutation of vertical crossover, the excessive local search capability of the algorithm can be alleviated. In the third phase, the horizontal crossover is considered as an operator to boost explorative trend by diminishing the unreachable search spot. Moreover, to accelerate the convergence speed, the competitive operator conducts greedy selection after performing each crossover. The introduction of three operators in CSO into HHO can enhance the equilibrium between exploratory and exploitative tendencies in case of an accelerated convergence speed and unchanged computational complexity. Furthermore, to access the effectiveness of CCHHO, we take a series of comprehensive experiments from three kinds of issues using 4 categories of benchmark functions, 3 well-regarded engineering optimization tasks and feature selection problems from 13 UCI datasets. On the global optimization tasks of benchmark functions, to show the superiority of the proposed optimizer more rigorously, the performance of the improved optimizer on the global optimization problems of benchmark functions is, respectively, compared with that of nine well-known bioinspired optimizers and that of nine advanced algorithms. 9 well-known bioinspired optimizers contains DE [19], PSO [8], SCA [20], GWO [21], MFO [22], WOA [23], B) [24], GSA [25] and CSO [50], which is used as a strategy in the developed algorithm. 9 advanced algorithms consist of LSHADE_cnEpSin [58], SaDE [59], LSHADE [60], CGPSO [61], CLPSO [62], ALCPSO [63], ACWOA [64], IWOA [65], and CCNMHHO [49], which is the variant of HHO based on Nelder-Mead simplex. And then the scalability evaluation and
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sensitivity analysis of CCHHO are conducted. Besides that, the CCHHO optimizer is compared with some other previous engineering optimizers when dealing with engineering optimization problems. On feature selection, the modified HHO is discretized to construct a feature selection method, which is evaluated by comparing with other feature selection techniques including CCNMHHO. The experimental results reveal that the proposed CCHHO is significantly more effective than HHO, CSO, CCNMHHO and other competitors on diverse categories of functions, and its advantage is not influenced by the increase of problems’ dimensions. Additionally, the results also illustrate that the proposed CCHHO outperforms some existing optimizers in working out engineering design optimization; for feature selection problems, it is superior to other feature selection methods including CCNMHHO in terms of fitness, error rate and length of selected features. Notably, the proposed CCHHO in this study and CCNMHHO both adopt the horizontal crossover and vertical crossover of CSO, while CCNMHHO is modified one more strategy, Nelder-Mead simplex, than CCHHO be. Notwithstanding, the results reveal that CCNMHHO is not only less effective than CCHHO on handling the global optimization and feature selection problems but also higher computational expense than CCHHO because of the extra strategy.

The main contributions of this paper are summarized as followed:

1. An effective variant of HHO, CCHHO, is presented by introducing the vertical and horizontal crisscross of CSO into the original HHO to handle global optimization, engineering optimization and feature selection problems.
2. The proposed algorithm utilizes the dimensional mutation of vertical crossover in CSO to avoid the stagnancy in local optima, the horizontal crossover in CSO to reduce the unreachable search spots and strengthen the exploratory capability. It improves the balance between exploration and exploitation capability. Furthermore, the convergence rate is accelerated using competitive operator.
3. The performance of the proposed CCHHO is investigated by addressing 4 categories of benchmark functions chosen from 23 classical function and CEC2014 and 4 constrained engineering optimization tasks.
4. The developed CCHHO is adopted to develop a binary feature selection technique for dealing with feature selection problems on 13 datasets.
5. The proposed CCHHO outperforms CCNMHHO, which is based on the strategies of CSO and Nelder-Mead simplex, in terms of performance and computational expense on the global optimization and feature selection problems.

The remainder of this paper is organized as follows: Sect. 2 explains the background of HHO and CSO and demonstrates the main structure of the proposed algorithm. And Sect. 3 provides the evaluations of the proposed approach using a set of experiments and analysis on global benchmark problems. The practicality of the proposed method in dealing with engineering optimization problems are verified in Sect. 4. Section 5 gives the application of the proposed optimizer on feature selection. Finally, conclusions and future work are drawn in Sect. 6.

2 Literature Study

The advantage of a stochastic optimization algorithm can be determined by whether the algorithm can appropriately harmonize its two significant characteristics: exploration and exploitation [66]. Nevertheless, the randomness of the stochastic optimizers leads to their drawbacks including premature convergence, poor diversity and imbalance between exploratory capability and exploitative capability [9]. Therefore, many studies were devoted to developing a novel excellent algorithm or improving an existing algorithm for solving a variety of optimization problems, which is always a challenging task [67].

As a novel bioinspired algorithm, HHO has been already paid more and more attentions on many application fields. At the very beginning, HHO was applied in the area of energy efficiency. EHHO [36] was first proposed based on chaotic strategy for closing the best solution and opposition-based theory for exploration. It is investigated on parameter estimation of photovoltaic model such as single diode module (SDM), double diode module (DDM), photovoltaic (PV) model and the manufacture’s datasheet. Experimental results demonstrated that EHHO is superior to the well-regarded competitors such as BLPSO, CLPSO, IJAYA and GOTBLBO in terms of not only root mean square error (RMSE) but also convergence speed for identifying the parameters of SDM, DDM and PV model. It also revealed that EHHO can be a beneficial approach to identify the parameters of solar cells in case of some harsh outdoor environment with high irradiance or low temperature. For the same study cases of the PV parameter extraction, Liu et al. [49] proposed an improved HHO, named CCNMHHO, using the Nelder-Mead simplex as well as the horizontal and vertical crossover of the CSO. CCNMHHO employed CSO to improve the population quality by enriching the information exchange between individuals and avoid the local optima by preventing the dimensional stagnation of individuals. Additionally, the Nelder-Mead simplex facilitated enhancing individual searching abilities in aspects of the local search phase and the acceleration of convergence. Experimental results revealed that CCNMHHO was very competitive in...
estimating the unknown parameters of diverse PV models when comparing to some state-of-the-art methods such as IJAYA, GOTLBO, MLBSA, CPSO, ABSO, ABC, CPSO, EHHO, and so on. And it performed well in solving the complex outdoor environments with diverse temperature and radiance.

HHO has also been applied in satellite image. [39] presented a dynamic HHO (DHHO/M) as a new satellite image segmentation approach, which was incorporated with a dynamic control factor and mutation strategy. The proposed DHHO/M was more efficient to improve the search capability and escape from local optimum than HHO. And experimental results indicated that, in the aspects of fitness function evaluation, image segmentation effect and statistical tests, the DHHO/M-based thresholding approach outperformed original HHO, the advanced multilevel thresholding methods including TLBO, WOA-TH, IDSA and BDE as well as the thresholding approaches based on different criteria such as Tsallis entropy based MG OA, MABC, Otsu-based MFPA and GWO. Furthermore, the practicality and feasibility on real engineering problems of DHHO/M was evaluated using four oil pollution images.

In addition, there are also some classification model optimizations using HHO. In [41], HHO provided a strengthened performance to optimize the artificial neural network (ANN) for improving the accuracy of ANN in predicting slope stability. Results illustrated that HHO raised the prediction accuracy of ANN in terms of RMSE and mean absolute error, and the correlation between actual values of the safety factor and the outputs of HHO-ANN was more significant than ANN. A HHO-CNN hybrid model for classifying hand gesture images was proposed in [44]. After tuning the hyper-parameter of CNN using HHO, the proposed model attained an accuracy of 100% and was superior to the existing models such as WOA-CNN, GSA-HHO, CSA-HHO, PSO-HHO, GA-HHO, ABC-HHO and GWO-HHO.

HHO also can be used in discrete optimization problems. An upgraded binary HHO, HHOSRL, [40] was proposed based on specular reflection learning (SRL) to accurately identify the decisive factors in the early recognition and discrimination of COVID-19 severity. Experimental results showed that the indicators HHOSRL selected, such as age, PaO$_2$, SaO$_2$, %, Na$^+$ and LAC, were essential for early accurate estimation of COVID-19 severity. Moreover, HHOSRL performed satisfactorily when fusing with various classifiers and achieved an accuracy of almost 100.0%. The kernel extreme learning machine enabled HHOSRL performed best on blood sample dataset. HHOSRL is the best feature selection method in terms of specificity, sensitivity, accuracy, MCC and time consumption when comparing with other feature selection techniques including bMFO, BGSA, bALO, BSSA, bHHO, bGWO, BPSO, BBA and bWOA. IHHO was proposed in [68], in which salp swarm algorithm was embedded in the update stage of HHO for solving global optimization and feature selection problems. The evaluation results of the proposed IHHO demonstrated that it provided a faster convergence rate and better performance on benchmark function optimization problems than 11 conventional swarm-based algorithms including HHO, DE, GWO, WOA, SSA, MFO, SCA, PSO, MVO, ALO, and GOA as well as 11 state-of-the-art optimizer such as JADE, SaDE, jDE, CoDE, SHADE, ALCP SO, CLPSO, BLPSO, HCLPSO, EPSO and HPSO-TVAC. The IHHO-based feature selection method outperformed BBA, BSSA and BH HO in respect of fitness, feature-length and error rate on ten benchmark feature selection issues. However, from the viewpoint of computational complexity, IHHO may spend much execution time. As set forth, the own characteristics and wide usage of HHO reflect the outstanding optimization capability. As a consequence, this study proposes a variant of HHO named CCHHO using CSO strategy. However, the CSO mechanism was also introduced in CCNMHHO. It should be noted that there are some differences between the proposed HHO and CCNMHHO. First, in addition to the CSO strategy, CCNMHHO used Nelder-Mead simplex as another mechanism. Second, CCHHO and CCNMHHO are not used in the same application field. The former is employed to handle global optimization, engineering optimization and feature selection problems, while the latter is used as a parameter extraction method of photovoltaic models. We will compare their performances in experiments on global optimization and feature selection problems in later sections.

3 Materials and Methods

3.1 Overview of HHO

HHO is a stochastic swarm intelligence optimizer. This optimizer imitates the collaborative behavior of Harris hawks’ swarm in hunting an escaping prey. The mathematical model is mainly based on two explorative phases and four exploitative processes, which are performed randomly. In HHO, the Harris’ hawks represent the search agents; the intended prey indicates the best or approximately optimal solutions obtained so far. In the explorative phases, Harris hawks randomly perch for locating prey. Two explorative phases are modeled based on the positions that hawks roosting. This pattern of exploration boosts the randomness of HHO. Accordingly, it is tending to enable the positions of search agents extend all over possible region of search space. While in the exploitative processes, once detecting the intended prey, the hawks attempt to employ four chasing strategies to cope with various escaping motions of the prey. Four chasing strategies are involved in four exploitative phases. In Appendix C of Supplementary material, Fig. C.1
draws each searching stage in HHO. Meanwhile, the detailed steps including the mathematical model of each stage are described as followed.

Step 1: Initialization.

The initial parameters such as population size N, maximum number of iterations T are determined. And the hawk population (search agents) \( X \) is defined randomly.

Step 2: Evaluation.

First, make sure that the current agent explores in the search space. In case of this, the best agent \( X_{\text{target}} \) is determined after evaluating the fitness of each search agent.

Step 3: Updating the escaping energy.

Due to the reducing escaping energy of the prey, the evolutionary process switches between exploration and exploitation. Obviously, the mutative energy greatly affects the optimization ability of HHO. This time-variant energy, marked as \( \text{Escaping}_{\text{energy}} \), is defined according to the following equations [26]:

\[
\text{Escaping}_{\text{energy}} = 2E_o(1 - \frac{t}{T})
\]

\[
E_o = 2rand - 1,
\]

where \( E_o \) represents random initial state, which is changed at each generation within the range \((-1, 1)\).

When \( |\text{Escaping}_{\text{energy}}| \geq 1 \), the search agent is updated by the explorative operation in Step 4, otherwise, when \( |\text{Escaping}_{\text{energy}}| < 1 \), the search agent is modified by the exploitative operation in Step 5.

Step 4: Exploration.

The search agent is distributed in various areas of the search space so as to explore the best agent. According to the equal probability \( q \), the position of the search agent is determined to be a random location when \( q \geq 0.5 \), while somewhere near other search agents enough when \( q < 0.5 \).

Therefore, there are two explorative phases expressed as Eq. 3 [26].

\[
X(t + 1) = \begin{cases} 
X_i(t) - r_1[X_i(t) - 2r_2X_i(t)], & q \geq 0.5 \\
(X_{\text{target}}(t) - X_{\text{average}}(t)) - r_3 \\
\times(r_4(UB - LB) + LB), & q < 0.5
\end{cases}
\]

\[
X_{\text{average}}(t) = \frac{1}{N}\sum_{i=1}^{N} X_i(t),
\]

where \( X_{\text{average}}(t) \) is the average position of the current search agents, \( X_i(t) \) represents the location of the \( i \)-th search agent at generation \( t \). \( X(t + 1) \) and \( X(t) \), respectively, indicate the position of search agents at generation \( (t + 1) \) and \( t \). \( X_i(t) \) denotes the position of a random agent. \( X_{\text{target}}(t) \) is the position of the best agent. \( r_1, r_2, r_3, r_4 \) and \( q \) are produced randomly between 0 and 1 at each generation.

Step 5: Exploitation.

According to different escaping status of the prey, four strategies for hawks are used in hunting the prey. Therefore, four exploitative processes are constructed to acquire the search agents around the global optimum produced so far. Besides the escaping energy, a random factor \( r \) in \((0, 1)\) is employed to determine which exploitative process is performed. In addition, \( \text{Jump}_{\text{strength}} \) represents the prey’s jump strength ought to be updated, it is calculated using the following equation [26]:

\[
\text{Jump}_{\text{strength}} = 2 \times (1 - \text{rand})
\]

(5)

The description and execution condition of each process is given below. Based on two factors: \( \text{Escaping}_{\text{energy}} \) and \( r \), one sub-step in Step 5.1–5.4 is chosen to complete the exploitation. It is remarkable that the soft besiege demonstrated in Step 5.1–5.2 occurs when \( |\text{Escaping}_{\text{energy}}| \geq 0.5 \) and the hard besiege described in Step 5.3–5.4 occurs when \( |\text{Escaping}_{\text{energy}}| < 0.5 \). Moreover, when \( r < 0.5 \) such as seeing Step 5.2 and Step 5.4, in both soft and hard besiege, the exploitative process can be the movement with progressive rapid dives, which is more intelligent because of the utilization of Levy flight.

\[
X(t + 1) = \Delta X(t) - \text{Escaping}_{\text{energy}}\times \\
\text{Jump}_{\text{strength}} \times X_{\text{target}}(t) - X(t)
\]

(6)

\[
\Delta X(t) = X_{\text{target}}(t) - X(t),
\]

(7)

where \( \Delta X(t) \) is the difference between the position of the best agent and the current search agents.

Step 5.2: The exploitative process can be modeled mathematically such that [26]:

\[
Y = X_{\text{target}}(t) - \text{Escaping}_{\text{energy}}\times \\
\text{Jump}_{\text{strength}} \times X_{\text{target}}(t) - X(t)
\]

(8)

\[
Z = Y + S \times \text{Levy}(D),
\]

(9)

where \( S \) is a random vector in the search space with size of \( 1 \times D \) and boundary of \([0, 1]\). Levy flight \( \text{Levy}(D) \) is used to evaluate the rapid dives [26].
\[
\text{Levy}(x) = 0.01 \times \frac{u \times \sigma}{|v|^{1/\beta}}, \quad \sigma = \left[ \frac{\Gamma(1+\beta) \sin(\pi \beta)/2}{\Gamma((1+\beta)/2) \times \beta \times 2^{\beta-1/2}} \right]^{1/\beta},
\]

where \(u, v\) are random factors and \(\beta = 1.5\). Finally, the search agents can choose their next movements using the following rule [26]:

\[
X(t + 1) = \begin{cases} 
Y, & \text{if } F(Y) < F(X(t)) \\
Z, & \text{if } F(Z) < F(X(t)) 
\end{cases},
\]

where \(F(\bullet)\) is the fitness evaluation function.

Step 5.3: The search agents are approximate to the best according to the following equation [26]:

\[
X(t + 1) = X_{\text{target}}(t) - \text{Escaping energy} \times |\Delta X(t)|.
\]

Step 5.4: In this process, all of the search agents are tended to be closer to the best agent. The search agent can be evaluated according to Eq. 13 [26].

\[
X(t + 1) = \begin{cases} 
Y', & \text{if } F(Y') < F(X(t)) \\
Z', & \text{if } F(Z') < F(X(t)) 
\end{cases},
\]

where

\[
Y' = X_{\text{target}}(t) - \text{Escaping energy} \times \text{Jump_strength} \times X_{\text{target}}(t) - X_{\text{average}}(t),
\]

\[
Z' = Y' + S \times \text{Levy}(D).
\]

Step 6: Repeat Steps 2–5 to perform optimization iteratively until the number of iterations has reached the iterative maximum.

Step 7: Obtain the optimal solution (\(X_{\text{target}}\)).

### 3.2 Overview of CSO

The population-based CSO is an efficient stochastic search optimizer with a crisscross search strategy based on the Confucian doctrine of golden mean. Incorporating a competitive (CP) operator with a dual crossover search behavior, which is different with the crossover in genetic algorithm, CSO algorithm can address the optimization problems, especially complex ones, with high-quality solution and accelerated convergence.

In the optimizing process of CSO, the dual crossover search behavior constructs an interacting chain of two searching operators, horizontal crossover (HC) operator and vertical crossover (VC) operator, respectively. HC is performed based on the capability of social recognition among individuals. While VC operation lies in the capability of each individual’s self-recognition. They are alternatively performed with respective probabilities to generate the moderation solutions in each iteration. After each crossover operating, CP operator is performed to estimate the moderation solutions (MS). The MS with better fitness values will be maintained in the new generation. The solutions reproduced in CP operator are referred to as dominant solutions (DS). DS are served as the parent population of the next HC or VC as well as the competitors of the MS stemming from one corresponding crossover operator. It is obvious that the population is modified twice in each iteration by HC and VC, respectively. And CP operator occurs twice to adjust the modified population.

The interacting process based on these operators in CSO can be illustrated in Fig. C.2. Each operator in CSO mentioned above is presented specifically as the following subsections. Suppose that the population \(X\) involving \(N\) search agents is trained in a D-dimensional search space. Then, the \(i\)-th search agent can be represented as \(X_i = [X_{i,1}, X_{i,2}, \ldots, X_{i,D}]^T, i = \{1, 2, \ldots, N\}\).

#### 3.2.1 HC operator

HC is a cross-border search mechanism. HC operator as a global optimization operator, randomly divides the population into two parts without repetition at first and then conducts a crossing over arithmetically on two distinct search agents across all their dimensions, which are, respectively, chosen from each subpopulation. After HC operation, each search agent is updated to be MS for HC. The following arithmetical model [50] can be used to express HC operation for a pair of different search agents at the \(d\)-th dimension.

\[
\left\{ \begin{array}{l}
MS_{\text{HC,}d} = r_1 \times X_{i,d} + (1 - r_1) \times X_{j,d} + c_1 \times (X_{i,d} - X_{j,d}) \\
MS_{\text{SH,}d} = r_2 \times X_{i,d} + (1 - r_2) \times X_{j,d} + c_2 \times (X_{i,d} - X_{j,d})
\end{array} \right.,
\]

where \(MS_{\text{HC,}d}\) and \(MS_{\text{SH,}d}\) represent the moderation solutions produced by HC, while \(X_{i,d}\) and \(X_{j,d}\) are their corresponding distinct parent search agents at the \(d\)-th dimension, which are employed to perform HC. \(r_1, r_2, c_1\) and \(c_2\) are random parameters that distributed uniformly, where the values of \(r_1\) and \(r_2\) are in \([0, 1]\); and \(c_1, c_2\) are considered as expansion coefficients in the range \([-1, 1]\). The expansive coefficients are very influential in determining the search scope of a search agent.

According to Eq. 16, in HC phase, the multi-dimensional search space is split into two parts. Each part is taken as a hypercube with the paired parent search agents as their diagonal vertices. As we can see in Eq. 16, each MS contains two components: the first component is originated from the arithmetical crossover in genetic algorithm, which ensures HC searching in each part of the separate hypercubes space with a larger probability; while the second
component applies the expansive coefficients, which ensures HC reducing effectively the unreachable blind spots by the first component and searching in the peripheral space of each part with a decreasing probability.

Additionally, to adequately reach the global search ability of HC operator, the HC probability \( P_h \) that HC operation occurs is set as 1. Within each generation, a CP operator performs a greedy selection after HC operation. The MS achieved by HC compete with the corresponding parents to produce DS as the new modified population. Accordingly, the survived DS are taken as the parent population of the following VC operation.

### 3.2.2 VC Operator

In VC operation, the information is exchanged between the paired dimensions of a search agent with VC probability \( P_v \). Performed in the opposite direction of HC’s horizontal direction, the VC operator randomly splits the dimensions of each parent search agent into two parts without repetition and then operates a crossing over arithmetically on all search agents between two diverse dimensions. The two distinct dimensions are, respectively, selected from each part of dimensions. The parent population is the population of DS derived from HC operation. After VC operation, each search agent is updated to be MS for VC.

Notably, considering that each dimension of search agent exists different units or different boundaries, the normalization and reverse normalization should be performed before and after the VC operation, respectively.

Before VC, the normalization operation on the parent search agents makes sure that the dimension offspring can be produced by VC within the boundary of each dimension. The normalized search agent can be calculated as below [50]:

\[
NX_{ij} = \frac{X_{ij} - LB_j}{UB_j - LB_j},
\]

where \( NX_{ij} \) represents the \( i \)-th normalized search agent at the \( j \)-th dimension. LB and UB are the minimum and maximum of the \( i \)-th search agent \( X_i \) at the \( j \)-th dimension, respectively.

VC operation on the paired dimensions of the \( i \)-th search agent can be shown as follows [50]:

\[
NV_{i,d1} = r \times NX_{i,d1} + (1 - r) \times NX_{i,d2}, \quad d1, d2 \in (1, D),
\]

where \( NV_{i,d1} \) indicates the moderation solution with normalized form generated by VC, while \( NX_{i,d1} \) and \( NX_{i,d2} \) are, respectively, corresponding parent search agents at the \( d1 \)-th and \( d2 \)-th dimension, which are adopted to execute VC. 

\( r \) is uniformly distributed parameter whose value is randomly generated in the range [0, 1].

After VC, the reverse normalization operation can be expressed by the following equation [50]:

\[
MSV_{ij} = NV_{ij} \times (UB_j - LB_j) - LB_j,
\]

where \( MSV_{ij} \) represents the moderated solution produced by VC operator.

From Eq. 18, VC search happens between two diverse dimensions of a single search agent and generates a single offspring. This exchange of dimensional information dramatically provides an opportunity to avoid dimensional stagnancy in population, hence it makes the stagnant dimension escape from local optimum without destroying other dimensions that may be the global optimum.

Since certain dimensions of the population may simultaneously encounter the premature convergence in optimization process, the VC probability \( P_v \), which determines the number of the paired dimensions taking part in VC operation, is set in \([0.2, 0.8] \) [50].

Similar to HC, after VC search operation, CP operation is also performed to generate DS as the new offspring population of the current population. It means that the outperformed DS are regarded as the parent population of HC search operation in the next generation.

### 3.2.3 CP Operator

As aforementioned, CP operator is applied to choose the better search agent after the population is updated by each crossover search. It plays a vital role in enhancing the search quality. CP operator employs a greedy selection mechanism to update the search agents, which can be expressed as below [50]:

\[
DS = \begin{cases} 
X, & \text{if } f(X) \text{ is better than } f(MS) \\
MS, & \text{if } f(MS) \text{ is better than } f(X)
\end{cases},
\]

where DS represents the new modified population for the next crossover operation, which are the better solutions with better fitness between MS generated by HC or VC and its parent \( X \).

From the arithmetical model of CP operator, only that MS who are superior to their parents can be survival, otherwise, they would be dropped out of the competition. The CP mechanism can simply make the search agents maintain the better solutions and converge to the global solution rapidly.

### 3.3 The Proposed CCHHO

In this subsection, with the aid of the separate inherent excellent abilities of the three operators in CSO, we construct an enhanced optimizer, referred as CCHHO, by incorporating
the operators into HHO. The structure of the proposed CCHHO is illustrated in Fig. 1, and its corresponding pseudocode is described in Appendix A of Supplementary material. The proposed CCHHO optimizer contains three phases: exploration, exploitation with dynamic adjustment, and enhanced exploration. Similar to the evolutionary process of each individual in the conventional HHO, in each generation, the escaping energy determines to perform the first exploration phase or the second exploitation phase. While the third phase optimizes all of the individuals produced from the first two phases in the current generation once more.

Exploration is the original exploration of HHO, which is divided into two stochastic exploring means based on the equal probability $q$. The search agents are randomly explored or searched around other search agents. This randomness is contributed to search the global optimal solution in an extensive search space. In this phase, a new exploring population is generated.

The exploitation with dynamic adjustment is to adjust the exploitation of the conventional HHO adaptively using a VC regulatory mechanism. The current search agent is modified through one of the four exploitation stages in the conventional HHO and recorded for the subsequent competition. Considering the possibility of premature convergence caused by the Levy flight in the preceding exploitation stages of HHO, VC search mechanism is employed to provide a dimensional mutation dynamically. The dimensional mutation is tended to make the stagnant dimension of a search agent jump out of the local optimum so as to boost the other stagnant dimensions to jump out of the local optimum as soon as possible. VC as an adjustment mechanism is performed in this phase with a certain vertical crossover probability after the preceding exploitation stages. As the architecture of VC search mechanism described in Fig. 2, the dimensions of each current search agent are split into two equal parts. And then a crossover is operated on paired dimensions. There is only part of dimension of the agent updated in resulting search agent. Similar to the VC in CSO, the CP operation is used to compete the resulting search agent with the recorded search agent. An adjusted population consists of the survival search agents. It is obvious that this VC mechanism integrated with CP operator can not only eliminate the local optimality caused by the dimensional stagnancy in previous exploitation stages but also achieve an improved stability between diversification and intensification.

Enhanced exploration is to perform HC search mechanism on all search agents as an enhanced global search operator. This phase is performed after updating the whole population in the first two phases. Therefore, the exploring or adjusted population originated from the above two phases is regarded as the parent population of HC operator. As demonstrated in Fig. 3, the population is split into two equal subpopulations. And a search agent is, respectively, chosen from each of the subpopulations. Each paired search agents are crossed...
based on HC mechanism. The same as HC in CSO, the CP operator is also introduced to perform a greedy selection between the resulting population of HC and its parent population. And then, the competitive individuals are addressed as the parent population of the next generation. In this phase, HC mechanism effectively facilitates to not only achieve the better solutions in different search spaces but also decrease the inaccessible scotoma, which cannot be obtained in the above two phases, in the solution space so as to boost the ability to search the global optimum. In this case, the excellent explorative ability of HC can fill the gap in the exploration of the conventional HHO. The enhanced exploration with HC mechanism improves the quality of the solution.

Moreover, we can see that the VC and HC with the CP operator introduced in the suitable phases of the evolutionary process of the proposed CCHHO can explore the high-quality global best solution for a faster convergence and a diversified population.

The complexity of CCHHO can be calculated based on the following five processes: initialization, exploration phase of HHO, the vertical crossover, horizontal crossover and competitive operator. First, for N search individuals, the computational complexity of initialization is \( O(N) \); Secondly, the computational complexity of exploration phase is \( O(T \times N \times D) \); third, the computational complexity of vertical crossover is \( \frac{1}{2} O(T \times N \times D) \); Fourth, the computational complexity of horizontal crossover is \( \frac{1}{2} O(T \times N \times D) \); finally, the competitive operator conducted after each crossover mechanism is \( 2O(T \times N) \). Therefore, the total computational complexity of CCHHO is \( 2O(N \times (T \times D + T + 1)) \), in which T is the maximum number of iterations and D is the dimension of the problem. It can be seen that the introduction of crisscross strategy into HHO makes the computational time increase one time, but does not rise the computational complexity.

4 Evaluations of the Proposed CCHHO

In this section, a series of experiments were conducted to investigate the efficiency and strength of incorporated mechanisms in the proposed CCHHO algorithm in a variety of cases. For all approaches in each experimental case, we recorded the fair results due to utilizing an identical experimental setup such as operating environment and parameter settings. All experiments are executed on Windows 10 (64 bit) operating system with Intel(R) Xeon(R) CPU E5-2680 v4 @ 2.40 GHz 2.39 GHz (two processors) and 8GBs RAM. The development tool MATLAB R2017a is used to code and run all algorithms. Considering evaluating the effectiveness of CCHHO optimizer from a more comprehensive perspective, the following experiments are conducted.

Experiment 1: Evaluating the performance of CCHHO on benchmark function optimization using four categories of benchmark functions. The tested functions contain three unimodal, three multimodal and three fixed-dimension multimodal test functions, which are chosen from 23 classical functions [69], as well as three composition functions available from IEEE2014 [70] test problems. The CCHHO is compared with 9 well-regarded bioinspired algorithms including HHO and CSO as well as 9 state-of-the-art optimizers including CCNMHHO on above 12 test functions. In addition, we perform the analysis of CCHHO’s performance with different dimension, different population size and different maximum iteration number.

Experiment 2: Evaluating the performance of CCHHO on engineering optimization problems such as tension/compression spring design, welded beam design and pressure vessel design. The optimization performance of CCHHO on these problems are compared with some existing engineering optimizer as well as CCNMHHO.

Experiment 3: Evaluating the CCHHO’s capability of tackling the feature selection problems on 13 UCI datasets. CCHHO as a feature selection approach is compared with 6 feature selection methods also including CCNMHHO.

4.1 Experiments on Global Optimization Problems

CCHHO is compared with 9 well-regarded optimizers and 9 state-of-the-art algorithms on 12 test functions, which are of different categories, including unimodal (F1–F3), multimodal (F4–F6), fixed-dimension multimodal (F7–F9) and composition (F10–F12) test functions. In Appendix B of Supplementary material, Table B.1 and Table B.2 show the mathematical descriptions of these benchmark functions. According to the own characteristics of each type of the problems, these functions were used to validate various properties of the proposed CCHHO algorithm. The unimodal and multimodal sets are suitable for examining the performance of the tested approach in terms of convergency, exploitative capability and explorative capability. Whereas, the rest test sets of CEC 2014 test functions were applied to evaluate the overall abilities of the tested algorithm to equilibrate exploration and exploitation.

In each experimental case, every chosen approach runs 30 times independently aiming at weakening the impact of randomness on experimental results. Also, the population size is set to 30. In computational intelligence, a matter of fact is the fairness of computational testing [71]. According this rule, we can make sure the obtained results are justifiably recorded without bias toward one or other algorithm [72]. The setup of initial parameters of all algorithms was identical with their original references. The setup of the parameters in all the comparing algorithms are recorded in Table 1.
Algorithm Parameters

CCHHO $c_1, c_2 \in [-1, 1]; x_1, x_2, \epsilon \in [0, 1]; p_1 = 1; p_2 = 0.6$
DE $F_{\text{min}} = 0.2; F_{\text{max}} = 0.8; CR = 0.1$
PSO $c_1 = 2; c_2 = 2; N_{\text{Max}} = 6$
SAC $a = 2$
GWO $a = [2, 0]$
MFO $b = 1; t = [-1, 1]; a \in [-1, -2]$
WOA $a_1 = [2, 0]; a_2 = [-2, -1]; b = 1$
BA $a = 0.5; \tau = 0.5$
GSA $G_0 = 100; a = 20$
CSO $c_1, c_2 \in [-1, 1]; x_1, x_2, \epsilon \in [0, 1]; p_1 = 1; p_2 = 0.6$
HHO $\text{RabbitEnergy} = [2, 0]$
LSHADE\_cnEpSin $\mu F = \mu CR = \mu freq = 0.5; H = 5; freq = 0.5; ps = 0.5; pc = 0.4$
SaDE $F_1 = 0.9, C_1 = 0.1; F_2 = 0.9, C_2 = 0.9; F_3 = 0.5, C_3 = 0.3; F_4 = 0.5, C_4 = 0.3; F_5 = 0.5, C_5 = 0.3$
L SHADE $r_{\text{ave}} = 18; r_{\text{ave}} = 2.6; p = 0.1; H = 6$
CGPSO $c_1 = c_2 = 1.49618; w = 0.7289$
CLPSO $w = [0.2, 0.9]; c = 1.496$
ALCPSO $c_1 = c_2 = 2.0; w = 0.4; G_0 = 60; T = 2; pro = \frac{1}{6}$
ACWOA $a_1 = [2, 0]; a_2 = [-2, -1]; b = 1$
IWOA $b = 1; \text{crossover} = 0.1$
CCNMMHO $c_1, c_2 \in [-1, 1]; x_1, x_2, \epsilon \in [0, 1]; p_1 = 1; p_2 = 1$

In this study, to estimate the optimization capability of the comparative algorithms, the statistical performance measures such as standard deviation and mean, which can be used to show the robustness of the examined algorithm, are employed to record the experimental results. In the table recording the experimental results, the “mean” and “std” label represent, respectively, the average value and standard deviation of 30 independent runs for each function. Moreover, we employed several extensive statistical significance results to evaluate the success of CCHHO. The Wilcoxon signed rank test at the significant level of 0.05 was applied to analyze statistically the significant difference of statistical measures among the comparative methods. In each Wilcoxon signed rank test result, the results of the significant analysis are shown in the description identified by “+/- =/−”, in which “+” represents the number of functions that CCHHO is superior to other tested methods significantly, whereas, “−” represents the number of functions that CCHHO is worse than others significantly, “=” represents the number of functions that the significant difference does not exist between CCHHO and other comparing methods. For further statistical analysis, we employed the Friedman test to present the average ranking performance of each tested method more evidently. The “ARV” label represents the average performance ranking of the algorithm based on Friedman test for overall benchmark functions. The “rank” label represents the overall ranking of each algorithm. The best results are bolded in the experimental results.

4.1.1 Comparison with Well-regarded Bioinspired Algorithms

In this subsection, nine well-regarded bioinspired algorithms were used to assess the efficiency of the proposed CCHHO. This comprehensive group of algorithms contains DE [19], PSO [8], SCA [20], GWO [21], MFO [22], WOA [23], BA [24], GSA [25] and CSO [50]. In this experimental case, the maximum number of function evaluations is set to 30,000.

Table B.3 expresses the statistical outcomes of comparing the developed CCHHO with the selected methods on tackling 12 benchmark functions. The p-values of Wilcoxon signed-rank test and Friedman test are used to assess the efficiency of the proposed CCHHO. From the outcomes of each methods listed in Table B.3 and Table B.4, it is obviously that CCHHO can achieve the best solutions on all of the functions. For F1–F3, the optimal solutions of F1, F2 are able to be found by CCHHO. While other competitors including CSO cannot obtain the optima. It indicates that CCHHO inherits the excellent exploitative
ability of original HHO, CSO and other compared optimizers are prone to premature convergence. For F4–F5, CCHHO outperforms other competitors except CSO. There are no significant difference between the performances CCHHO and CSO on F4–F6. This reveals that CCHHO gets the good explorative ability of CSO to escape from local optima. For F7–F9, CCHHO performs worse than CSO and DE on F7, equal with CSO on F9. However, CCHHO also can get the best solution on each function. For F10–F12, CCHHO is significantly superior to other comparing algorithms including CSO, which shows that CCHHO can achieve a better equilibrium between exploration and exploitation than others.

Observing from Table 2, the overall statistical outcomes of significance in Wilcoxon signed rank test demonstrate that CCHHO produces 7 significantly better/4 equal/1 significantly worse when compared with CSO, which is the worst case. And CCHHO performs significantly worse than DE, WOA and CSO on only 1 function, equal with CSO and GWO on, respectively, 4 functions and 1 function. This indicates that CCHHO has overwhelmingly advantages over other approaches. It makes sense that CCHHO achieved the best ARV of 1.5292 in the Friedman test, which outperforms CSO in second place with ranking value of 2.3333. Therefore, we can draw the conclusion that the developed CCHHO was the best method with considerable success over 9 well-established bioinspired algorithms.

The curves in Fig.C.3 intuitively shows the convergence rate of CCHHO, DE, PSO, SCA, GWO, MFO, WOA, BA, GSA and CSO on addressing eight functions. As we can detected from Fig.C.3, CCHHO converges faster with the best solution than other competitors on all functions except F9. CCHHO achieves a competitive convergence rate on F9. It approaches the best solutions later than CSO, but it attains the best solution, which is not significantly different with the solution obtained by CSO. For other competitors, their accelerated trends are tend to stagnate into local optimum during early evolutionary stage, whereas CCHHO can converge fastest with the high-quality solutions on these optimization tasks. Therefore, based on the enhanced exploratory trends of HC operator, the convergence speed of CCHHO is also boosted. It is obvious that these tendencies can confirm the enhancement of CCHHO in most cases of the unimodal, multimodal and composition problems.

In summary, these overall results on each type of problems verify that the proposed HHO has a steadily efficient evolutionary capability at an accelerated convergence rate. This indicates that, in CCHHO, the HC mechanism facilitates strengthening the global search capability; the reasonable adjustments of HC and VC mechanisms are able to successfully make an excellent balance between exploitation and exploration trends; and the CP operator is helpful to boost the convergence rate.

### 4.1.2 Comparison with State-of-the-Art Algorithms

In this subsection, the advantages of the proposed CCHHO were investigated by comparing against several state-of-the-art optimization algorithms such as LSHADE_cnEpSin [58], SaDE [59], LSHADE [60], CGPSO [61], CLPSO [62], ALCPSO [63], ACWOA [64], IWOA [65], CCNMHHO [49]. In this experimental case, the maximum number of function evaluations is set to 45,000. Table B.5

| Metric | CCHHO | LSHADE_cnEpSin | SaDE | LSHADE | CGPSO | CLPSO |
|--------|--------|----------------|------|---------|--------|-------|
| +/=-/- | 11/01  | 9/21           | 10/2 | 12/00  | 6/376  | 5/823 |
| ARV    | 2.2861 | 5.8014         | 4.931 | 5.7625  | 6.736  | 5.823 |
| Rank   | 1      | 5              | 3    | 4       | 8      | 6     |
| Metric | ~      | ALCPSO         | ACWOA | IWOA   | CCNMHHO|
| +/=-/- | ~      | 10/20          | 8/40 | 12/00  | 8/40   | 8/40  |
| ARV    | ~      | 6.6514         | 6.117 | 7.3583  | 3.8944 |
| Rank   | ~      | 9              | 7    | 10      | 2      |
records the relevant mathematical results in terms of the statistical metrics, Wilcoxon statistical test and Friedman test. The p values in Table B.6 demonstrate the statistical significance at 5% degree of the Wilcoxon test between the proposed CCHHO and each competitor. Table 3 provides the significant statistical results from Wilcoxon signed-rank test and Friedman test. Figure C.4 visibly illustrates the afore mentioned results in terms of the convergence rate.

As observed in Table B.5, CCHHO can exhibit the best performance on all twelve functions except F8. On unimodal cases, the CCHHO has an excellent ability of exploitative search due to finding the optimal solutions on F1, F2 and the best solution on F3, while the ACWOA, as the second top exploitative algorithm on unimodal problems, achieves the optimal solution on F1 and F2. But ACWOA cannot attain a satisfactory solution on F3. Moreover, CCNMHHO is less effective than CCHHO, which indicates that the exploitative ability of CCHHO has an excellent ability of exploitative performance on all twelve functions except F8. On unimodal cases, the CCHHO obtains the best solutions on all unimodal functions, while the CLPSO and CCNMHHO can achieve the best solutions only on F5 and F6. This observation reveals that the enhanced explorative ability of CCHHO outperforms other methods. In other words, the integrating the Nelder-mead simplex may not boost the explorative capability of CCNMHHO. On the fixed-dimension cases, the performance of CCHHO is competitive to other comparing algorithms. CCHHO obtains the best solution on F7, which is not significantly different with LSHADE_cnEpsin, SaDE, LSHADE, CLPSO, ALCPSO and CCNMHHO. Moreover, according to the standard deviation, CCHHO is more stable than CCNMHHO and ALCPSO. For F8, CCHHO performs worse than SaDE, but it also can attain the best solution. For F9, CCHHO is superior to all other algorithms. For the composition functions, CCHHO is significantly superior to other splendid algorithms including CCNMHHO. As we can see that the coordination between exploration and exploitation of CCHHO is the best of that of all comparing algorithms.

According to the significant statistical results in Table 3, CCHHO performs 11/9/10/12/9/10/8/12/8 significantly better, 1/2/2/0/3/2/4/0/4 equal, 0/1/0/0/0/0/0/0/0 significantly worse when comparing with LSHADE_cnEpsin, SaDE, LSHADE, CGPSO, CLPSO, ALCPSO, ACWOA, IWOA, CCNMHHO. Accordingly, from each perspective, the performance of CCHHO outperforms the selected outstanding competitors. Although the ACWOA also has a nice exploitative capability and SaDE and CLPSO can perform a relatively good explorative search, these are only single advantage for them. Furthermore, the results of Friedman test reveal that CCHHO ranks the first among ten algorithms, followed by CCNMHHO, SaDE, LSHADE, LSHADE_cnEpsin, CLPSO, ACWOA, CGPSO, ALCPSO, IWOA. Therefore, although CCNMHHO can achieve an excellent performance, the Nelder-mead simplex in this method weakens its exploitative capability, and then makes the coordinate between exploration and exploitation worse than CCHHO.

Figure C.4 exposes the above merits of the proposed CCHHO by means of convergence curves. According to the curves, we detect that the convergence rate of CCHHO is accelerated on several functions including F1, F3, F4, F5, F11. It is also obvious that most of other advanced competitors occurs premature convergence on F1, F3, F4, F5, F11, F12. For F7, F9, F12, CGPSO traps into the local optimum with faster convergence than CCHHO, which can converge to the best solutions. These trends indicate that the convergence rate of CCHHO is accelerated in searching the global solution. Notably, the CCHHO has a faster convergence speed than CCNMHHO on each function. It confirms that CCHHO can effectively harmonizes the high search ability and accelerated convergence rate.

The numerical results and convergence curves indicate that CCHHO outperforms the other comparing state-of-the-art optimizers with higher convergence rate. Therefore, it makes sense that the HC and VC mechanisms of CSO are contributed to enhancing the CCHHO’s performance comprehensively and effectively.

Accordingly, the comprehensive effectiveness of the proposed CCHHO is the best among all comparing optimizers. First, CCHHO can provide high explorative capability due to combing the horizontal crossover into the later evolutionary stage of HHO. Second, CCHHO has strong exploitation ability resulting from the reasonable integration of the excellent exploitative ability of HHO’s levy flight and the adjustment of vertical crossover. Third, CCHHO attains an accelerated convergence speed. Finally, the experimental results verify that the proposed CCHHO has a suitable coordination between exploration and exploitation with the help of the CSO strategy. Hence, CCHHO has a better effectiveness than CCNMHHO, which is also improved using CSO strategy, on coping with the global optimization problems. In other words, employing more mechanisms may not enhance the optimization performance of the algorithm. In the next subsections, the effectiveness of CCHHO will be verified in some more challenging real problems such as engineering optimization and feature selection.

4.1.3 Scalability Evaluation

Above subsections presented the merits of the proposed CCHHO by comparing with other well-established and advanced methods. This section provides a scalability evaluation to analyze the impact of dimensions of
the optimization task on the efficiency of CCHHO. In this evaluation, the CCHHO algorithm was compared against the original HHO on six benchmark functions with increasing dimensions of 100, 200, 500, 1000 and 2000, respectively. Table B.7 reports the statistical results for each dimension of six optimization cases tackled by CCHHO and HHO.

As Table B.7 demonstrated, the comparison results on each dimension are very stable to show the superiority of the CCHHO to HHO. On each dimension, the proposed CCHHO can attain the same optimal or best solutions as HHO when addressing all functions. However, the CCHHO significantly outperforms HHO on the same magnitude when tackling F3, F5, F6. Hence, observing from the standard deviations, CCHHO is significantly more stable than HHO on any dimension. For F1, F2, F4 and F6, both of CCHHO and HHO achieve the optimal or best solution whatever the dimension is. It means that the optimization ability of the proposed CCHHO is enhanced on the problems in different dimensions due to the combination of two crisscross operations. And the success of the proposed method is not affected by the increasing dimensions of the optimization problems. In addition, it can be known that CCHHO produces the best performance when dimension is 2000, and the worst on dimension of 500.

4.1.4 Sensitivity Analysis

Since majority of metaheuristic algorithms perform on a general idea, rather than provide particular domain knowledge for each problem, diverse values of parameters set for an algorithm may result in diverse performance [73]. It is necessary to identify the parameter settings for algorithm and then can provide robustness and applicability in handling a variety of problems in different scientific areas. The performance of the proposed CCHHO is sensitive to the initial parameter such as the population size (N) and maximum number of iterations (T). A sensitivity analysis is done to examine the impact of these two parameters on CCHHO. For the sensitivity analysis, N is set to {30, 50, 80, 100} and T is set to {100, 500, 800, 1000}. The analysis is conducted using these parameters on functions selected from four categories of unimodal, multimodal, fixed-dimension multimodal and composition test functions in Table B.1 and Table B.2. They are, respectively, F3, F5, F8 and F10. For each function, the maximum number of function evaluation is 30000. The sensitivity analyzing results are shown in aspects of mean and convergence rate for the four functions.

First, from the perspective of population size (N), CCHHO is simulated for different population size and fixed number of iterations. The iteration number is fixed to 1000. Table B.8 gives the average fitness values of CCHHO on F3, F5, F8, F10 with four different population size. It reveals that CCHHO obtains the best performance with a small population size. Additionally, from the convergence curves of CCHHO on F5 related with different population size in Fig. C. 5(a), the sensitivity of CCHHO decreases with population size.

Second, from the perspective of maximum number of iterations (T), CCHHO is executed for different number of iterations. Table B.9 recorded the average fitness values of CCHHO on F3, F5, F8, F10 with four different number of iterations. Figure C. 5(b) presents the convergence curves of CCHHO on F5 with different number of iterations. It can be detected from Table B.9 and Fig.C. 5(b) that CCHHO converges to optimal solution with the increasing of the number of iterations. It shows that the iterations number is essential to the convergence and robustness of CCHHO.

4.2 Applications to Engineering Optimization Problem

The reliability of the proposed CCHHO can be assessed on solving the real-world engineering optimization problems. In this subsection, CCHHO is employed to tackle three well-known engineering optimization tasks, which are tension/compression spring design [74], welded beam design [74] and pressure vessel design [74, 75] problem. The outcomes of optimization for solving each engineering problem were compared to a variety of standard and advanced methods proposed in previous literature.

4.2.1 Tension/Compression Spring Design Problem

The objective of the tension/compression spring design problem is to minimize the weight of a spring by determine the optima of three structural variables such as wire diameter (d), the number of active coils (N) and mean coil diameter (D). The mathematical definition of this case is as follows [74]:

Consider \( \bar{x} = [x_1, x_2, x_3] = [d, N] \), Min. \( f(\bar{x}) = (x_3 + 2)x_2^2 + x_1^2 \). (21)
Subject to \( g_1(\vec{x}) = 1 - \frac{x_2^3x_3}{71785x_1^4} \leq 0, \)
\[
g_2(\vec{x}) = \frac{4x_2^2 - x_1x_2}{1256(x_2x_1^3 - x_1^4)} + \frac{1}{5108x_1^7} \leq 0, \]
\[
g_3(\vec{x}) = 1 - \frac{140.45x_1}{x_2^2x_3} \leq 0, \]
\[
g_4(\vec{x}) = \frac{x_1 + x_2}{1.5} - 1 \leq 0 \]

Variables range \( 0.05 \leq x_1 \leq 2, 0.25 \leq x_2 \leq 1.30, 2.00 \leq x_3 \leq 15 \)

The tension/compression spring design problem is one of the most ordinary engineering optimization problems. It has already been employed to verify the effectiveness of the new optimizers in many studies. The proposed CCHHO is compared with several recent well-established methods including OBLGOA, BWOA, IFFOA, IGWO, PSOCSCLF, CMSSA, RW-GWO, RGWO, FCMHMD, HHO and CCNMHHO. CCNMHHO is coded for this problem. The results shown in Table 4 point out that the proposed CCHHO and FCMHMD can find the optimal variables for this problem with the weight of 0.1266523. The CCNMHHO, BWOA, HHO, IFFOA, CMSSA, which achieve competitive results, are respectively, ranked in the 2nd, 3rd, 4th, 5th and 6th places.

### 4.2.2 Welded Beam Design Problem

The main aim of this well-known case is to design a welded beam to determine four decision variables that minimize the fabrication cost. The decision variables include the weld thickness \( (h) \), length of an attached part of the bar \( (l) \), height of the bar \( (t) \) and thickness of the bar \( (b) \). The mathematical definition of this case can be expressed by the following [74]:

Consider \( \vec{x} = [x_1x_2x_3x_4] = [htlb] \).

Min. \( f(\vec{x}) = 1.10471x_1^2x_2 + 0.04811x_3x_4(14.0 + x_2) \). (22)

Subject to \( g_1(\vec{x}) = r(\vec{x}) - r_{max} \leq 0, \)
\[
g_2(\vec{x}) = \sigma(\vec{x}) - \sigma_{max} \leq 0, \]
\[
g_3(\vec{x}) = \delta(\vec{x}) - \delta_{max} \leq 0, \]
\[
g_4(\vec{x}) = x_1 - x_4 \leq 0, \]
\[
g_5(\vec{x}) = P - P_c(\vec{x}) \leq 0, \]
\[
g_6(\vec{x}) = 0.125 - x_1 \leq 0, \]
\[
g_7(\vec{x}) = 1.10471x_1^2x_2 + 0.04811x_3x_4(14.0 + x_2) - 5.0 \leq 0 \]

Variables range \( 0.1 \leq x_1, x_4 \leq 2, 0.1 \leq x_2, x_3 \leq 10 \)

Where \( r(\vec{x}) = \sqrt{(r')^2 + 2r'r''x_2^2} \),
\[
r' = \frac{P}{\sqrt{2x_1x_2}}, \]
\[
r'' = \frac{MR}{J}, \quad M = \frac{P}{2}(L + \frac{x_2}{2}), \quad R = \frac{x_2}{2} + \frac{1}{4}, \quad J = 2\left\{ \sqrt{2x_1x_2} \frac{x_2}{4} + \left( \frac{x_1 + x_4}{2} \right)^2 \right\}, \]
\[
\sigma(\vec{x}) = \frac{6PL}{x_4x_3^2}, \quad \delta(\vec{x}) = \frac{6PL^2}{E_4x_3^4}, \]
\[
P_c(\vec{x}) = \frac{40118}{E_4} \frac{x_2^4}{36} \left( 1 - \frac{x_3}{2L} \sqrt{E \over 40G} \right). \]

\( P = 6000lb, \quad L = 14in, \quad r_{max} = 0.25in, \quad t_{max} = 13, 600psi, \quad \sigma_{max} = 30, 000psi, \quad E = 30 \times 10^6psi, \quad G = 12 \times 10^6psi \)

The welded beam design problem has been extensively handled by various optimizers such as BSAISA, BWOA,
OBLGOA, CMSSA, G DFA, CG WO, V CS, C-ITGO, IAHLO, SFO, SFS, HHO, FCMHMD, SSC and RGWO. To evaluate the ability of the proposed CCHHO in addressing this engineering design case, the estimated variables and optimal cost obtained by this optimizer are compared against those of these optimizers and CCNMHHO. The detailed comparison results listed in Table 5 reveal that the proposed CCHHO algorithm is able to identify the best design for this engineering case by attaining the optimal cost of 1.69526617. This cost is the lower than that of other algorithms. CCNMHHO finds the optimal cost of 1.69527319, which is higher than CCHHO.

### 4.2.3 Pressure Vessel Design Problem

The main purpose of pressure vessel design problem is to design the cylindrical pressure vessel with a minimum total cost, which contains the cost of materials and welding. To tackle this case, four parameters \( (T_s, T_h, R, L) \) must be optimized. \( T_s \) and \( T_h \) denote the thickness of the shell and head, respectively; \( R \) is the inner radius; \( L \) represents the length of the cylindrical section of the vessel without head. The mathematical model of this case can be defined as follows [74]:

Consider \( \bar{x} = [x_1, x_2, x_3, x_4] = [T_s, T_h, R, L] \),
\[
\text{Min. } f(\bar{x}) = 0.6224x_1x_2x_3 + 1.7881x_2x_3^2 + 3.1661x_1^2x_4 + 19.84x_2^2x_3,
\]

### Table 5 Overall results of welded beam design problem

| Optimizer       | Optimal variables | Optimal cost   |
|-----------------|-------------------|----------------|
| BSAISA [81]     | 0.205730 3.470489 9.036624 0.205730 | 1.724852       |
| BWOA [76]       | 0.205829 3.251922 9.034556 0.205829 | 1.695620       |
| OBLGOA [3]      | 0.205769 3.471135 9.032728 0.2059072 | 1.7257         |
| CMSSA [82]      | 0.205113 3.261434 9.036661 0.2057296 | 1.724700       |
| G DFA [83]      | 0.205670 3.472000 9.036680 0.205730 | 1.724700       |
| CG WO [84]      | 0.343891 1.883570 9.03133 0.212121 | 1.725450       |
| V CS [85]       | 0.20572964 3.47048867 9.03662391 0.20572964 | 1.695838       |
| C-ITGO [86]     | 0.20572964 3.47048867 9.03662391 0.20572964 | 1.72485231     |
| IAHLO [87]      | 0.205730 3.470489 9.033624 0.205730 | 1.724852       |
| SFO [66]        | 0.2038 3.6630 9.0506 0.2064 | 1.73231        |
| SFS [88]        | 0.20572964 3.47048867 9.03662391 0.20572964 | 1.72485231     |
| HHO [26]        | 0.204039 3.51061 9.027463 0.206147 | 1.73199057     |
| FCMHMD [74]     | 0.2056756 3.47090936 9.043817 0.205693 | 1.725684       |
| SSC [89]        | 0.1992 3.4307 9.1045 0.2051 | 1.7222         |
| RGWO [9]        | 0.20569 3.4718 9.0365 0.20574 | 1.7253         |
| CCNMHHO         | 0.20571349 3.253420735 9.036575827 0.205731928 | 1.69527319     |
| CCHHO           | 0.20572195 3.253272321 9.03656748 0.20573221 | 1.69526617     |

### Table 6 Overall results of pressure vessel design problem

| Optimizer       | Optimal variables | Optimal cost   |
|-----------------|-------------------|----------------|
| OBLGOA [3]      | 0.81622 0.40350 42.291138 174.811191 | 5966.67160     |
| RW-GWO [80]     | 0.81250 0.43750 42.09840 176.63784 | 6059.736       |
| OBSCA [90]      | 1.2500 0.0625 59.1593 70.8437 | 5833.9892      |
| MHDA [91]       | 0.778169 0.384649 40.3196 200 | 5885.3353      |
| WOA [23]        | 0.812500 0.437500 42 0.0982699 176 0.638999 | 6059.7410      |
| HHO [26]        | 0.81758383 0.4072927 42.09174576 176.7196352 | 6000.46259     |
| FCGHMMD [74]    | 0.8129 0.401571 42.087015 176.85321 | 5952.89502     |
| CCNMHHO         | 0.942465189 0.46586103 48.83293932 107.8873575 | 5833.620039    |
| CCHHO           | 0.94877596 0.46898044 49.15937475 105.15766782 | 5826.47696325  |
Some optimization algorithms previously utilized to tackle the pressure vessel design problem include OBLGOA, RW-GWO, OBSCA, MHDA, WOA, HHO and FCGHMD. The performance of the CCHHO algorithm on optimizing this design problem is compared with that of these algorithms and CCNMHHO. The comparison outcomes in Table 6 report the optimal cost of 5826.47696325. It reveals meaningfully that the CCHHO is the most effective optimizer among above well-established ones in this engineering design case.

According to the analysis of the above three constrained engineering optimization tasks, the proposed CCHHO has confirmed its efficiency in addressing real-world engineering optimization problems over other well-regarded optimizers. It indicates that the superiority of CCHHO results from the HC and VC operators that interact reasonably with the HHO mechanism. Also, due to the constrained property and uncertain search space in the engineering optimization problems, we can see that CCHHO can perform optimization in the search domain with infeasible spaces.

### 4.3 Application to Feature Selection

Feature selection (FS), as an optimization process of dimensionality reduction, is an essential stage of addressing the high-dimensional search space in classification problem. In this section, the proposed CCHHO is used in dealing with this challenging process for further assessing the availability of CCHHO in real-word application. FS problem aims at determining a subset with the fewest representative features from the overall set of properties in original dataset to achieve an optimal classification accuracy. Therefore, as the architecture of FS based on a binary optimizer illustrated in Fig. 4, it is observed that the classification accuracy of the classifier can be considered as the measurement of validating the ability of dimensionality reduction.

#### 4.3.1 FS Based on Binary CCHHO

The FS problem can be taken as a discrete optimization problem. Therefore, the proposed CCHHO is transformed into a binary version, called BCCHHO, since the solved FS task is characterized as a binary optimization problem. Hence, in the implementing process of CCHHO for solving FS problem, the continuous solutions are mapped into discrete forms with binary value. The solution ought to be represented as a binary vector with the same dimensions as the number of features in the training dataset. In the vector with binary values, the selected attribute is labelled with value 1 at its corresponding location, whereas the non-selected attribute is marked with value 0.

First, we produced binary values in accordance with random thresholds to initialize the population as followed:

\[
x_{ij} = \begin{cases} 
0 & \text{rand} \leq 0.5 \\
1 & \text{rand} > 0.5 
\end{cases}
\]

(24)

where \(x_{ij}\) denotes the binary value in the location vector of search agent at \(i\)-th row and \(j\)-th column.

Second, without influencing the architecture of CCHHO, we can employ the transfer function to map the continuous vector of search agent into binary form in the formal transformation. In this study, we chose the S-shaped transfer function [92], shown as Eq. 25, to perform the mapping to squash the continuous vectors in each dimension.

\[
S_{\text{Trans}} = \frac{1}{1 + e^{-x_{ij}/3}}.
\]

(25)
where $x$ represents the continuous vector of search agent. $S_{\text{Trans}}$ denotes a continuous intermediate form as the output of the transfer function. To achieve a binary vector, $S_{\text{Trans}}$ is changed and compared with the initial binary vector generating in the initialization based on the following equation [68]:

$$
x_{i,j} = \begin{cases} 
\text{outputPos} = \text{initialPos rand} \leq S_{\text{Trans}} \\
\text{outputPos} = \text{initialPos rand} > S_{\text{Trans}}
\end{cases}.
$$

where initialPos is the initial binary value, outputPos indicates the new binary value attained.

Finally, we applied the classifier to evaluate the selected subset of features obtained from BCCHHO. FS is evidently regarded as a multi-objectives problem since it involves acquiring the highest classification accuracy with fewest feature subsets. Therefore, considering the objectives comprehensively, we can evaluate the search agent in accordance with the classification accuracy and the number of chosen features using the fitness function as follows [68]:

$$
\text{fitness} = \alpha \times \left(\frac{N_{s}}{N}\right) + \beta \times (1 - \text{accuracy}),
$$

where $N_{s}$ denotes the number of features filtered by BCCHHO. $N$ is the total number of features in original dataset. accuracy represents the classification accuracy calculated from the classifier. $1 - \text{accuracy}$ indicates the error rate. $\alpha$ and $\beta$ are considered as the weights of the selected features’ number and classification accuracy, respectively, $\alpha \in [0, 1]$, $\beta = 1 - \alpha$. They represent the importance of the selected features’ number and error rate.

### 4.3.2 Experimental Setup

We present a comparative study to examine the optimization behavior of the binary CCHHO compared to several state-of-the-art bioinspired algorithms including BHHO (binary HHO [26]), bGWO [93], BBA [94], bWOA (binary WOA [23]), BSSA (binary salp swarm algorithm [95]) and BCCNMHHO, which is the binary versions of CCNMHHO [49] improved using CSO and Nelder-mead simplex. Thirteen practical benchmark datasets on distinct subject areas were utilized as case studies. They are available from the UCI repository (https://archive.ics.uci.edu/ml/datasets.php, available at October 2022) and the Wielaw dataset is from the literature [96]. As presented in Table B.10, in these datasets, the sizes of instances and features are distinguished with each other. That is beneficial to assess the proposed method from distinct perspectives.

To alleviate the bias of feature selection, in the training of classification, k-fold cross-validation (CV) is employed to assess the optimality of each selected feature subset. The dataset in k-fold CV was segmented into $k$ equivalent parts. One part in the dataset is used as the testing set to estimate the classifier’s classification accuracy, while the $k-1$ parts is the training set for training the classifier. The evaluation...

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### Table 7 Comparison results of the proposed BCCHHO vs. other optimizers in aspect of fitness

| Dataset | BCCHHO | BHHO | bGWO | BBA | bWOA | BSSA | BCCNMHHO |
|---------|---------|------|------|-----|------|------|----------|
| ARV     | 1.9385  | 6.4846 | 2.4308 | 6.5077 | 4.0308 | 4.6115 | 1.9962   |
| Rank    | 1       | 6    | 3    | 7   | 4    | 5    | 2        |

### Table 8 Comparison results of the proposed BCCHHO vs. other optimizers in aspect of error rate

| Dataset | BCCHHO | BHHO | bGWO | BBA | bWOA | BSSA | BCCNMHHO |
|---------|---------|------|------|-----|------|------|----------|
| ARV     | 2.2538  | 5.7308 | 2.3462 | 7   | 4.2346 | 4.0500 | 2.3846   |
| Rank    | 1       | 6    | 2    | 7   | 5    | 4    | 3        |

### Table 9 Comparison results of the proposed BCCHHO vs. other optimizers in aspect of feature-length

| Dataset | BCCHHO | BHHO | bGWO | BBA | bWOA | BSSA | BCCNMHHO |
|---------|---------|------|------|-----|------|------|----------|
| ARV     | 2.3923  | 5.7077 | 3.5654 | 5.2423 | 2.8731 | 5.8615 | 2.3577   |
| Rank    | 2       | 6    | 4    | 5   | 3    | 7    | 1        |

### Table 10 Comparison results of the proposed BCCHHO vs. other optimizers in aspect of computational time

| Dataset | BCCHHO | BHHO | bGWO | BBA | bWOA | BSSA | BCCNMHHO |
|---------|---------|------|------|-----|------|------|----------|
| ARV     | 5.8462  | 5.1538 | 2.3000 | 3.1308 | 1.6077 | 2.9615 | 7        |
| Rank    | 6       | 5    | 2    | 4   | 1    | 3    | 7        |
metrics of FS are the average values obtained from \( k \) validation for each problem.

For fairness in the investigation, each evaluation associated with the BCCHHO is performed in the same computational environment. The initial parameters of all comparison methods were identical with that in their original references. Furthermore, for each involved method, the search agents and maximum iteration are, respectively, set as 20 and 50. It runs ten independent times. And the common KN was used as classifier in training. The fold \( k \) in k-fold CV was set as 10, and \( \alpha \) is 0.05 [68, 97].

We adopt four evaluation metrics to express the experimental results. They are the average fitness, average error rate, average number of the selected features and average computational time. Moreover, the corresponding standard deviation (std) is accompanied in the results to estimate the performances of the investigated FS approaches on thirteen datasets on ten independent runs. According to the selected features subsets in the evaluated datasets, the average fitness and average error rate are attained. Additionally, the average ranking value (ARV) in aspects of the evaluation metrics based on the Friedman test are employed to detect the optimal solutions among the examined optimizers. The best values of four evaluation metrics are bold in the results.

### 4.3.3 Results and Discussion

The simulation results attained by BCCHHO against other competitors are recorded in Table B.11, 12, 13, 14 in aspects of average fitness, error rate, numbers of selected features as well as computational time, respectively. Tables 7, 8, 9, 10 demonstrate the average ranking results of all investigated optimizers based on Friedman Test.

Observing the results of average fitness in Table B.11, BCCHHO shows competitive outcomes of average fitness. The proposed optimizer can attain the best average fitness on 7 of 13 datasets, while BCCNMHHO and bGWO get the best solution on 5 and 4 datasets, respectively. However, the average fitness obtained by BCCHHO are very close to the best value. Considering Table B.11, 12, 13, BCCHHO can achieve the lowest error rate with relatively fewer features on Exactly, M-of-n, WineEW, Zoo, vehicle, wdbc and Wielaw. On other datasets, bGWO and BCCNMHHO can obtain the best fitness. Nevertheless, the lowest error rates are mostly attained by bGWO at the cost of selecting more features. And BCCNMHHO cannot realize the lowest error rates, which indicates that BCCNMHHO have missed the important information that affect the accuracy because of selecting the fewest features. This also can be concluded from Tables 7, 8, 9. According the average ranking value based on Friedman test, BCCHHO is ranked first in terms of average fitness and error rate. BCCNMHHO ranks in the first position in terms of feature-length, but it cannot outperform BCCHHO in terms of the two important metrics such as fitness and error rate.

Inspecting the computational time shown in Table B.14 and Table 10, BCCNMHHO expends the most running time among the tested algorithms, followed by BCCHHO, BHHO. However, as the variants of the original HHO, BCCNMHHO takes more than three times as long as that of HHO. It can be known that the time expend of BCCNMHHO is influenced by the introduced Nelder-mead simplex and CSO strategies. The computational expend of BCCHHO is the second most expensive, nevertheless, it is close to that of HHO and less half of BCCNMHHO’

As summary, the BCCHHO can achieve the best fitness and the lowest error rate with relatively fewer features on the datasets with low-dimensional as well as high-dimensional datasets. This indicates that the proposed BCCHHO provides a remarkable success among the tested FS techniques. It can be obviously concluded that the proposed BCCHHO considerably overcomes the limitations of the original version of BHHO by integrating the HC and VC operators. This optimizer is suite for the discrete feature selection problem. Additionally, the above analysis of the computational time reveals that the computational time of an algorithm is affected by its mechanism of finding optimum.

### 5 Conclusions and Future Directions

In this study, an enhanced HHO (CCHHO) optimizer was proposed, in which the horizontal crossover strategy in CSO is fused with the update stage of HHO, the vertical crossover strategy in CSO is introduced into the exploitation phase of HHO and the competitive operator in CSO is also performed after each crossover. The combination of CSO in HHO ensures not only a good balance between local search capability and global search ability but also an accelerated convergence speed. The CCHHO’s performance is comprehensively assessed on four categories of functions. The results show that CCHHO is more efficient than other well-known bioinspired algorithms and advanced optimizers in terms of convergence and the balance between exploitation and exploration. Simultaneously, on solving the engineering optimization problems, the CCHHO outperforms other previous optimizers to lower manufacturing costs. Hence, for the FS problems, binary CCHHO achieves higher accuracy by selecting fewer features than other competitors. In a word, CCHHO can handle continuous global optimization problems and discrete feature selection with an outstanding effectiveness. Additionally, we detect that CCHHO is
superior to CCNMHHO on solving the above problems. It indicates that the Nelder-mead simplex introduced in CCNMHHO may not be contributed to achieving the best efficiency when addressing these problems, while it increases the algorithm’s computational time. Consequently, it is not always the case that more strategies added into an algorithm can make it perform better. Moreover, an algorithm cannot be a universal method for solving every problem, which is proven by “NFL” theorem.

Accordingly, we can attempt to evaluate what other problems the CCHHO can work out. In this study, we adopt the CCHHO in single objective problems and low-dimensional feature selection. As a future study, the CCHHO can be used for multi-objective optimization problems and high-dimensional feature selection such as gene selection. Additionally, due to its verified excellent capability of optimization and applicability in feature selection, we can also employ it to enhance the classifier’s accuracy by optimizing its key parameters and simultaneously selecting the optimal feature subsets.

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**Availability of Data and Materials** The data involved in this study are all public data, which can be downloaded through public channels.

**Declarations**

**Conflict of interest** The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

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