BLACK HOLE MASS ESTIMATES AND RAPID GROWTH OF SUPERMASSIVE BLACK HOLES IN LUMINOUS $z \sim 3.5$ QUASARS

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ABSTRACT

We present new near-infrared (IR) observations of the H$\beta$ $\lambda$4861 and Mg $\Pi$ $\lambda$2798 lines for 32 luminous quasars with $3.2 < z < 3.9$ using the Palomar Hale 200 inch telescope and the Large Binocular Telescope. We find that the Mg $\Pi$ FWHM is well correlated with the H$\beta$ FWHM, confirming itself as a good substitute for the H$\beta$ FWHM in the black hole mass estimates. The continuum luminosity at 5100 Å well correlates with the continuum luminosity at 3000 Å and the broad emission line luminosities (H$\beta$ and Mg $\Pi$). With simultaneous near-IR spectroscopy of the H$\beta$ and Mg $\Pi$ lines to exclude the influences of flux variability, we are able to evaluate the reliability of estimating black hole masses based on the Mg $\Pi$ line for high redshift quasars. With the reliable H$\beta$ line based black hole mass and Eddington ratio estimates, we find that the $z \sim 3.5$ quasars in our sample have black hole masses $1.90 \times 10^9 M_\odot \lesssim M_{BH} \lesssim 1.37 \times 10^{10} M_\odot$, with a median of $\sim 5.14 \times 10^9 M_\odot$ and are accreting at Eddington ratios between 0.30 and 3.05, with a median of $\sim 1.12$. Assuming a duty cycle of 1 and a seed black hole mass of $10^4 M_\odot$, we show that the $z \sim 3.5$ quasars in this sample can grow to their estimated black hole masses within the age of the universe at their redshifts.

Key words: black hole physics – galaxies: active – quasars: emission lines – quasars: general

1. INTRODUCTION

Active galactic nuclei (AGNs) are generally accepted to be powered by the gravitational potential energy extracted from matter falling toward a supermassive black hole (SMBH). The scaling relations between central black hole (BH) masses and various properties of their host galaxy spheroidal components, such as bulge mass, luminosity, and stellar velocity dispersion, strongly suggest that BH growth is coupled with galaxy formation and evolution (Gebhardt et al. 2000; Ferrarese & Merritt 2000; Onken et al. 2004; Nez et al. 2004; Kormendy & Ho 2013). The observed luminosity function and BH mass function at different redshifts reveal a downsizing phenomenon, whereby more massive BHs underwent their active accretion in earlier cosmic time; the comoving number density of massive active BHs peaks at earlier time than the less massive active BHs (Ueda et al. 2003; Richards et al. 2006; Vestergaard et al. 2008; Vestergaard & Osmer 2009; Kelly et al. 2010, 2012; Shen & Kelly 2010, 2012; Kelly & Shen 2013). Combination of the BH mass function with the luminosity function can better constrain the growth of SMBHs and their connections with the galaxy evolution (Vestergaard et al. 2008; Kelly et al. 2012). Reliable BH mass estimates are of fundamental importance in determining the BH mass functions and understanding other physical processes related to BHs.

In the local universe, BH mass estimates of Seyfert 1 galaxies and quasars have been done successfully with the reverberation mapping (RM) technique, mainly involving the H$\beta$ line (e.g., Kaspi et al. 2000; Peterson et al. 2004; Bentz et al. 2010; Barth et al. 2011; Grier et al. 2012, 2013). Based on these results, tight empirical correlations between the broad line region size and the continuum or emission line luminosity in optical wavelength have been established (Kaspi et al. 2000, 2005; Wu et al. 2004; Peterson et al. 2004; Bentz et al. 2006, 2009, 2013).

Assuming that the broad line region gas is virialized (Peterson & Wandel 1999, 2000; Peterson et al. 2004), these correlations have been widely adopted to estimate the BH masses of low redshift AGNs with single-epoch optical spectra based on the H$\beta$ line (Greene & Ho 2005; Vestergaard & Peterson 2006; McGill et al. 2008; Vestergaard & Osmer 2009). In the shorter ultraviolet (UV) wavelength range, such estimates have also been extended to the cases of the Mg $\Pi$ $\lambda$2798 or C iv $\lambda$1549 emission line based BH masses for small samples of AGNs (Vestergaard 2002; McLure & Dunlop 2004; Warner et al. 2004; Vestergaard & Peterson 2006; Kong et al. 2006; Kollmeier et al. 2006). These scaling relations are important for estimating the BH masses of high redshift AGNs because the H$\beta$ line moves out of the optical window and we have to rely on the Mg $\Pi$ and C iv emission lines for AGNs at $z > 0.7$. The Mg $\Pi$ and C iv lines have been adopted to estimate BH masses for a large sample of Sloan Digital Sky Survey (SDSS) quasars and to study the BH growth history (Vestergaard 2004; Shen et al. 2008). However, the reliability of the BH mass estimates based on the Mg $\Pi$ and C iv emission lines is still controversial, compared to the H$\beta$ line based estimates (Baskin & Laor 2005; Netzer et al. 2007; Trakhtenbrot & Netzer 2012). Some studies have confirmed the consistency (Vestergaard & Peterson 2006; Shen et al. 2008; Wang et al. 2009; Shen & Liu 2012), but some proposed additional calibrations to reduce the deviations from the H$\beta$ line based BH mass estimates (Denney 2012; Park et al. 2012, 2013; Denney et al. 2013).

At high redshift, the H$\beta$ line shifts to the near-IR window. Thus, with the near-IR spectroscopy, we can still directly use the well established empirical relation involving the H$\beta$ line to obtain the BH masses for high redshift quasars. Shen et al. (2004) and Netzer et al. (2007) obtained H and K band spectroscopy of the H$\beta$ line and derived BH masses of $10^{8.8}$–$10^{10.7} M_\odot$ for 44 quasars with redshift between 2.2 and
3.4. Dietrich et al. (2009) obtained J and H band spectroscopy for 10 quasars with redshift between 1.0 and 2.2 and derived Hβ line based BH masses of $10^{9.3} - 10^{10} M_\odot$. Greene et al. (2010) used the TriSpec of the 3.5 m telescope at Apache Point Observatory to obtain near-IR spectroscopy of 16 lensed quasars with redshift between 1.0 and 3.6 (only one at $z > 3$) and derived Hβ and He line based BH masses of $10^{8.8} - 10^{9.9} M_\odot$. Trakhtenbrot et al. (2011) presented H band spectroscopy of 40 AGNs with redshift around 4.8 and obtained Mg II line based BH masses of $10^{8.5} - 10^{10.5} M_\odot$. Shen & Liu (2012) investigated the reliability of UV virial mass estimates for a sample of 60 quasars at $1.5 < z < 2.2$ and obtained Hβ line based BH masses of $10^{9.5} - 10^{9.7} M_\odot$. In addition, near-IR spectra have also been taken for some $z \sim 6$ quasars, and BH masses of $10^{8.5} - 10^{9.7} M_\odot$ were obtained using the Mg II and C IV lines (Willott et al. 2003; Jiang et al. 2006; Kurk et al. 2007; De Rosa et al. 2011).

From these studies we can see that there still exist some redshift gaps ($z \sim 3.5$) without reliable Hβ line based BH mass estimates. More importantly, based on multi-epoch spectra of 615 high redshift quasars selected from the SDSS, the uncertainties of BH mass estimates due to inherent variability are estimated to be $\sim 30\%$ (Willi et al. 2007). All of the previous studies investigated only a single emission line (either Hβ or Mg II) in the near-IR bands; simultaneous high-quality observations of both Hβ and Mg II lines for $z \sim 3.5$ quasars have rarely been done. However, this is essential in obtaining a reliable calibration between the Hβ and Mg II line based BH masses at high redshift; in this case, the only factor influencing the calibration is the intrinsic difference between these two simultaneously observed emission lines. Therefore, with this goal in mind, we have observed a sample of quasars with $3.2 < z < 3.9$ using the Palomar Hale 200 inch telescope and the Large Binocular Telescope (LBT). Our spectroscopy in the J, H, and K bands from 0.8–2.2 μm covers the Mg II, Hβ, and Fe II lines simultaneously, allowing us to critically examine the reliability of the BH mass estimates based on the Mg II line.

In this paper, we present a brief overview of our sample, observations and data reduction in Section 2 and describe the method of spectral fitting in Section 3. We investigate correlations between spectral properties in Section 4 and present modified calibration results based on the rest-frame UV emission lines in Section 5. The results are discussed in Section 6. The main results are summarized in Section 7. We adopt $\Omega_M = 0.7$, $\Omega_\Lambda = 0.3$ and $H_0 = 70$ km s$^{-1}$ Mpc$^{-1}$ throughout the paper.

2. SAMPLE, OBSERVATIONS, AND DATA REDUCTION

We select our targets from the SDSS DR7 quasar catalog (Shen et al. 2011; Schneider et al. 2010) mainly by constraining the redshift and magnitude ranges. The redshift range ($3.2 < z < 3.8$) ensures that both the Hβ and Mg II lines are well covered in our near-IR spectroscopy. Certain redshift ranges where the Hβ or Mg II lines fall in telluric absorption bands in the near-IR windows are avoided. We further restrict the Two Micron All Sky Survey (2MASS; Skrutskie et al. 2006) J and K magnitude to brighter than 17.0 and 16.0 mag, respectively.

As part of the Telescope Access Program in China, 30 targets were observed during 2010–2012 with the TriSpec instrument mounted on the Palomar Hale 200 inch telescope. TriSpec is a cross-dispersed near-IR spectrograph providing continuous spectral coverage of 0.95–2.46 μm simultaneously at a resolution of $\sim 2700$ (Herter et al. 2008). A slit width of 1" was used during observations, and the targets were nodded along the slit to obtain good background subtraction. Another two quasars were observed with the LUCI I near-IR instrument (Hill et al. 2012) mounted on the LBT. LUCI I is a near-IR imager/spectrograph for the LBT with wavelength coverage of 0.85–2.4 μm (zJHK bands) in imaging, long-slit and multi-object spectroscopy modes. The spectra were taken with the N1.8 camera and the 210 l/mm J, 210 l/mm K gratings, yielding a spectral resolution of 1.5 Å. The total integration time in each band for each target is typically 2400–3600 s. A0V type stars were observed either before or after our targets at similar airmass, to remove telluric features in the following data reductions. Our sample and the follow-up observations are summarized in Table 1, where the systemic redshifts measured from their [O III] $\lambda 5007$ lines are also listed. For all these targets, there are good SDSS spectra covering C IV $\lambda 1549$ with mean signal-to-noise ratio (S/N) per spectral resolution element (3 pixels) greater than 10.

Reduction of the raw spectroscopic data from TriSpec is carried out using the modified IDL-based Spextool3 package (Cushing et al. 2004). After the flat field correction using the lamp spectra, observations in different nodded positions are pair-subtracted to remove most of the background. For each target, all the individual exposures are wavelength calibrated and extracted to be one-dimensional spectra, which are then combined to get the final averaged spectrum and telluric corrected. The sky background subtraction, flat correction, and wavelength calibration of the raw spectra from the LBT have been done with the modified IDL longslit reduction package for NIRSPEC (Becker et al. 2009; Bian et al. 2010). After this step, the one-dimensional spectra are extracted using the IRAF and then telluric corrected in the same way with that for the TriSpec data. Special attention is paid to telluric correction, where each extracted quasar spectrum is divided by a telluric spectrum. The telluric spectrum is obtained from dividing the observed A0V stellar spectrum by a scaled and reddened model Vega spectrum according to the observed magnitudes of the A0V star. Before this step, the model Vega spectrum is convolved with a function that broadens the lines to the observed widths and smooths it to the observed resolution (Cushing et al. 2004). The best obtained telluric spectrum is then visually examined, with removing those broad emission or absorption lines by manually scaling their equivalent widths. The absolute flux calibration is done by comparing the 2MASS JHK band magnitudes with the synthetic JHK band magnitudes. These synthetic magnitudes are obtained by convolving the quasar spectrum with the 2MASS response function provided by Cohen et al. (2003). The final spectra are also corrected for the Galactic extinction (Cardelli et al. 1989; Schlegel et al. 1998) and the wavelength is redshift corrected to the rest frame.

3. SPECTRAL MEASUREMENTS

For each emission line (Hβ and Mg II) in the near-IR spectroscopy, we fit a pseudo-continuum to the wavelength range around the line. The pseudo-continuum consists of a power-law continuum and Fe II template without including the contribution from Balmer continuum, because the Balmer continuum is difficult to be constrained from the noisy spectra in the gap between the J and H bands. The exclusion or inclusion of the Balmer continuum does not significantly influence the decomposition of broad lines (Shen & Liu 2012). However, they also stated that it may affect the continuum luminosity measurement by $\sim 0.12$ dex. Note that this factor is omitted.
in our estimate of luminosity measurement uncertainties. After subtracting the pseudo-continuum, the emission lines are fitted with multiple Gaussians. The emission line fitting process is briefly described as follows (see Shen et al. 2011 for more details).

We fit the wavelength range of 4700–5100 Å with two Gaussians for the broad Hβ component, one Gaussian for the narrow Hβ component, and two Gaussians for the [OⅢ] λ5007 and [OⅢ] λ5007 narrow lines. The line center offset from its theoretical value (namely the line shift) and the FWHM of the spectral lines are thus considered to be the corresponding uncertainties. As stated in Shen et al. (2011), the flux density uncertainty of the broad component and one Gaussian for the narrow component in the rest-frame wavelength range 1500–1600 Å with two Gaussians for the broad component and one Gaussian for the narrow component.

For the C iv emission line in the SDSS optical spectra, we fit the wavelength range 1500–1600 Å with two Gaussians for the broad component and one Gaussian for the narrow component. The narrow component is freely fitted with an upper limit of 1200 km s$^{-1}$.

An example of the continuum and emission line fitting is shown in Figure 1. Similar to Shen & Liu (2012), a Monte-Carlo approach is applied to estimate the uncertainties of the fitting parameters. For each object, 50 random mock spectra are created by introducing random Gaussian noises to the original spectrum; at each pixel in a given mock spectrum, the noise term is randomly drawn from a normal distribution with the observed flux density error as the standard deviation. We then fit the mock spectra with the same fitting strategy. The 1σ dispersions of the measured C iv FWHM vary from 500 km s$^{-1}$ to 1200 km s$^{-1}$.
Figure 1. Example of our model fits to the near-IR spectrum of SDSS J094202.04+042244.5. Here $\lambda_{rf}$ refers to the rest-frame wavelength. Top panel: the observed spectrum is shown as the solid black line. The model (solid red line) is composed of power-law continuum (blue dashed line), Fe $\text{II}$ template and Gaussian fits to emission lines, such as the Mg $\text{II}$, H$\beta$ and [O $\text{III}$] lines. Bottom panels: the red lines show the combined model fitting of Mg $\text{II}$ and H$\beta$. In each panel, the purple ones refer to the two Gaussians of the broad component and their combined profile is shown in green; the blue lines represents the model fits for their narrow components and the brown lines show the fitting residuals.

mock spectrum is increased compared to the original one, since they are added twice. Nevertheless, these mock spectra can still be considered to represent the wavelength-dependent noise properties.

The fitting results, such as emission line widths and continuum luminosities, are listed in Table 2. For quasars labeled as “good” (see the next section for details), the spectra together with their best-fit models of the Mg $\text{II}$ and H$\beta$ lines are shown in Figures 2 and 3, respectively.

4. CORRELATIONS OF SPECTRAL PROPERTIES

After excluding six broad absorption line quasars (BALs) from the 32 quasars, we calculate the median S/N per spectral resolution element (3 pixels) for each quasar over the whole spectroscopy. It is difficult to identify line features from the spectrum with S/N less than 10. Based on the criteria, J232735.67-091625.6 is labeled as “poor” with S/N $\sim$ 8.1. Another target J012403.77+004432.6 at redshift of 3.834 is also labeled as “poor” (despite its high median S/N as 70), because its Mg $\text{II}$ and H$\beta$ emission lines are located in the gap between J and H and the gap between H and K bands, respectively; the accurate determination of the line profiles is prevented under this circumstance. For the three quasars without good telluric corrections due to the bad weather during the observations, we label their quality as “median.” Therefore, based on the remaining 21 quasars labeled as “good,” we proceed to investigate the correlations between widths of different lines and between continuum or emission line luminosities at different wavelengths, as well as those between their virial products.

To describe the rank correlation between different parameters, such as the FWHMs of different emission lines, we estimate the Spearman rank correlation coefficient $r_1$ and the probability $p$ of its deviation from the null hypothesis that there is no relationship between the analyzed parameters. Correlations with $r_1 > 0.5$ are referred as strong. Those with $0.3 < r_1 \leq 0.5$ are considered as intermediate. Those with $0.1 < r_1 \leq 0.3$ are referred as weak and those with $r_1 < 0.1$ are considered as none or very weak. Correlations with the probability $p$ less than 0.05 (confidence level larger than 95%) are considered as significant. As suggested by Wang et al. (2009), consistent results can be obtained from most of the regression methods with or without errors, including the ordinary least-squares (OLS) method, FITexy (Press et al. 1992), the bivariate correlated errors, and intrinsic scatter (BCES) regression method (Akritas & Bershady 1996). To perform a more comprehensive regression analysis on the spectral properties, we apply a commonly used OLS method (without errors) and the BCES method (with errors) to our sample. Though there is no prior knowledge about which of the two variables is independent, the BCES method, treating the two variables symmetrically, can yield reasonable results (Akritas & Bershady 1996; Wang et al. 2009). Accompanied by the regression analysis, the Pearson product-moment correlation coefficient $r_2$ is also calculated to illustrate the strength of the proposed regression relationship.
These correlation coefficients are calculated and the regression fittings are performed only for the targets labeled as "good," although the quasars labeled as "median" are also shown in Figures 4 and 5. Especially for the correlations between proper-

4.2. Luminosity Correlations

In Figure 5, we compare different luminosities with the continuum luminosity at 5100 Å ($L_{5100}$). The results are listed in Table 3. Because our objects are luminous ($10^{47.5}$ erg s$^{-1}$ > $L_{5100}$ > $10^{46.0}$ erg s$^{-1}$), the contribution to $L_{5100}$ from the host galaxy is negligible (Shen et al. 2011; Shen & Liu 2012). This luminosity range complements the local $L_{5100}$-$L_{3000}$ relation at the brighter end.

In the literature, the continuum luminosity at 1350 Å ($L_{1350}$) or the continuum luminosity at 3000 Å ($L_{3000}$) is often used in the absence of $L_{5100}$ to estimate the BH masses based on UV spectra. The luminosities of broad emission lines are sometimes used, if the continuum is either too faint or contaminated by radiation from host galaxy or relativistic jets (Wu et al. 2004; Greene & Ho 2005; Shen et al. 2011; Shen & Liu 2012).

We find strong correlations between $L_{1350}$ and broad line luminosities, i.e., $L_{H\beta}$ and $L_{Mg\,\beta}$. Their Spearman correlation coefficients are 0.79 ± 0.04 and 0.48 ± 0.04, respectively, with confidence levels higher than 95%. The correlation between $L_{3000}$ and $L_{5100}$ is strongest, yielding $r$ of 0.84 ± 0.01. These relations indicate that either luminosity can be used to estimate BH masses.

5. A MODIFIED VIRIAL BH MASS ESTIMATE

As shown in Sections 4.1 and 4.2, scatters in the line width correlations and the luminosity correlations can introduce uncertainties in BH mass estimates. Simultaneous observations of the Mg ii and Hβ lines in our near-IR spectroscopy provide a unique opportunity to assess the reliability of the BH mass estimates for high redshift luminous quasars based on the Mg ii line.
Figure 2. Fitting results of the Mg\textsc{ii} lines for the 20 targets labeled as “good” and with full coverage of the Mg\textsc{ii} line. Note that the two targets (J0804 and J2130) have truncated profiles, but due to their acceptable Mg\textsc{ii} line fitting, we still take them as objects with full coverage of Mg\textsc{ii}. The spectrum in each panel is shown as the black line. The red lines show the combined model fitting of the emission line, where the purple ones refer to the two Gaussians of the broad component and their combined profile is shown in green; the blue lines represent the model fits for the narrow components and the brown lines show the fitting residuals.

| Correlations of Spectral Properties | \( r \) | \( p \) | \( r \) | slope\_OLS | Scatter (dex) | slope\_BCES |
|------------------------------------|------|------|------|------------|--------------|-------------|
| \( FWHM_{\text{H}\beta} \) vs. \( FWHM_{\text{Mg}\textsc{ii}} \) | 0.72 ± 0.10 | 0.00 ± 0.01 | 0.75 ± 0.11 | 1.09 ± 0.23 | 0.29 | 1.44 ± 0.33 |
| \( FWHM_{\text{C}\textsc{iv}} \) vs. \( FWHM_{\text{H}\beta} \) | 0.59 ± 0.01 | 0.01 ± <0.01 | 0.56 ± 0.01 | 0.69 ± 0.24 | 0.57 | 1.20 ± 0.38 |
| \( L_{5100} \) vs. \( L_{3000} \) | 0.48 ± 0.04 | 0.04 ± 0.02 | 0.67 ± 0.09 | 1.05 ± 0.28 | 0.73 | 0.96 ± 2.32 |
| Notes. Column 1: \( L_{\text{H}\beta} \), \( L_{\text{Mg}\textsc{ii}} \) and \( L_{\text{C}\textsc{iv}} \) refer to luminosities of broad components of the H\textsc{ii}, Mg\textsc{ii} and C\textsc{iv} lines, respectively. Column 2: Spearman rank correlation coefficient. Column 3: probability of \( r \) deviating from the null hypothesis. Column 4: Pearson’s correlation coefficient. Column 5: slope from the fit of their logarithmic values using the OLS method. Column 6: scatter perpendicular to the best-fitting linear relation using the OLS method. Column 7: slope from the fit of their logarithmic values using the BCES method.
We take the BH masses calculated based on FWHM$_{H\beta}$ and $L_{5100}$ using the calibration from Vestergaard & Peterson (2006) as the reference values. The virial BH mass estimates based on line width and luminosity can be expressed as

$$\log \left( \frac{M_{BH,\text{vir}}}{M_\odot} \right) = a + b \log \left( \frac{L}{10^{44} \text{ erg s}^{-1}} \right) + c \log \left( \frac{\text{FWHM}}{\text{km s}^{-1}} \right),$$

(1)

where $L$ and FWHM are the continuum (line) luminosity and width of one specific line, respectively. Coefficients $a$, $b$, and $c$ are obtained from the linear regression analysis.

Modified calibrations for Mg\textsc{ii} are derived from the 19 quasars labeled as "good" with full coverage of both emission lines (H\textsc{\beta} and Mg\textsc{ii}). We still assume that the broad line region gas is virialized. Thus, using the LINMIX\_ERR method (Kelly 2007), we fit the coefficients in Equation (1) under Scheme 1, where $a$ and $b$ are free parameters and $c$ is fixed at 2.0. The LINMIX\_ERR method is a Bayesian approach to linear regression with error in one independent variable. For comparison, another fitting scheme (Scheme 2) is applied to Equation (1) using the MLINMIX\_ERR method (Kelly 2007); in this case, $a$, $b$, and $c$ are all free parameters. The MLINMIX\_ERR is a Bayesian approach to linear regression with errors in multiple independent variables. The derived coefficients and their uncertainties are the mean values and the standard deviations of their distributions from the Bayesian analysis, respectively.

Based on the $z \sim 3.5$ quasars in our sample, the result of Scheme 1 is as follows:

$$\log \left( \frac{M_{BH,\text{vir}}}{M_\odot} \right) = (1.07 \pm 2.62) + (0.48 \pm 0.88) \log \left( \frac{L_{3000}}{10^{44} \text{ erg s}^{-1}} \right) + 2 \log \left( \frac{\text{FWHM}_{\text{Mg\textsc{ii}}}}{\text{km s}^{-1}} \right).$$

(2)

While for Scheme 2, the coefficients $a$, $b$, and $c$ are $4.95 \pm 1.67$, $0.25 \pm 0.31$, and $1.11 \pm 0.30$, respectively. These two modified calibrations are obtained from simultaneous observations of Mg\textsc{ii} and H\textsc{\beta} lines for 19 high redshift luminous quasars. However, given the small size and the narrow luminosity range of our sample, the uncertainties in the best-fit parameters are relatively large. Thus we note that the modified calibration may
Figure 3. Fitting results of the H\(\beta\) lines for the 20 targets labeled as “good” and with full coverage of the H\(\beta\) line. Colors of these lines have the same meaning with Figure 2.

not be the best for other studies. Here, the Mg\(\text{ii}\) based BH masses for our sample are estimated using Equation (2) and listed in Column 7 of Table 2.

6. DISCUSSION

6.1. Comparison with Earlier Studies

For the 19 quasars labeled as “good” and with full coverage of both the two emission lines (H\(\beta\) and Mg\(\text{ii}\)), based on the reliable reference BH mass estimates using the H\(\beta\) line, we find that the BH masses are between \((1.90 \pm 0.24) \times 10^9 M_\odot\) and \((1.37 \pm 0.04) \times 10^{10} M_\odot\). The median value is \(5.14 \times 10^9 M_\odot\) with the 1\(\sigma\) dispersion \(\sim 0.25\) dex.

The reference BH masses are compared with \(M_{\text{BH}}\) estimated from the Mg\(\text{ii}\) emission line based calibrations given in earlier studies, and the distributions of the offsets are shown as the black histograms in Figure 6. The red histogram refers to the distribution of the offsets between \(\log M_{\text{BH}}\) measured for our sample based on Equation (2) and the reference \(\log M_{\text{BH}}\). The Mg\(\text{ii}\) line-based BH masses estimated with Equation (2) range from \((1.01 \pm 0.69) \times 10^9 M_\odot\) to \((1.53 \pm 0.32) \times 10^{10} M_\odot\) with a median value of \(3.37 \times 10^9 M_\odot\). The 1\(\sigma\) scatter of these \(M_{\text{BH}}\) estimates away from the median value is \(\sim 0.37\) dex.

The measurement uncertainties of the Mg\(\text{ii}\) line-based \(\log M_{\text{BH}}\) are between 0.02 dex and 0.46 dex, with a median value of 0.07 dex. These measurement uncertainties can be significantly amplified, after including the large uncertainties in the fitted parameters in Equation (2).

Despite of large uncertainties in the best-fit parameters, the two newly derived calibrations from Scheme 1 and Scheme 2 still provide consistent BH mass estimates compared with the reference masses. The mean offsets from the reference \(M_{\text{BH}}\) are \(-0.01 \pm 0.27\) and \(-0.01 \pm 0.18\), respectively. The earlier studies and their calibrations based on FWHM\(\text{Mg\text{ii}}\) and \(L_{3000}\) are listed in the first four columns of Table 4. The last two columns show the comparison results, i.e., the mean offset of the estimated \(\log M_{\text{BH}}\) values from the reference \(\log M_{\text{BH}}\) and the 1\(\sigma\)
Table 4

| Ref. | $a$     | $b$     | $c$     | $z$     | Mean Offset (dex) | $\sigma$ (dex) |
|------|---------|---------|---------|---------|------------------|----------------|
| MD04 | 0.505   | 0.620   | 2.000   | 0.1–2.1 | $-0.17$          | 0.27           |
| VO09 | 0.860   | 0.500   | 2.000   | 0.08–2.5| $-0.17$          | 0.27           |
| W09  | 2.710   | 0.460   | 1.480   | 0.4–0.8 | $-0.30$          | 0.21           |
| S12  | 1.816   | 0.584   | 1.712   | 1.5–2.2 | $-0.17$          | 0.27           |
| K06  | 0.310   | 0.880   | 2.000   | 0.4–0.8 | $-0.17$          | 0.27           |
| T12  | 0.748   | 0.620   | 2.000   | 1.0–5.0 | $0.08$           | 0.27           |

Notes. Column 1: references of previous calibrations: MD04 (McLure & Dunlop 2004), VO09 (Vestergaard & Osmer 2009), W09 (Wang et al. 2009), S12 (Shen & Liu 2012), K06 (Kollmeier et al. 2006) and T12 (Trakhtenbrot & Netzer 2012). Columns 2–4: the values of $a$, $b$, and $c$ in Equation (1). Column 5: the redshift range of the sample utilized in references shown in Column 1. Column 6: the mean offset of the log $M_{\text{BH}}$ values estimated with the Mg $\text{ii}$ line-based calibrations away from the reference log $M_{\text{BH}}$ obtained using the H$\beta$ line-based calibration in Vestergaard & Peterson (2006). Column 7: the 1$\sigma$ uncertainty of the deviation from the mean offset.

![Figure 3](Continued)

In general, BH masses estimated with the calibrations from these earlier studies are consistent with the reference H$\beta$ based virial BH masses. Mean absolute offsets shown in Column 6 of Table 4 are between (0.01 ± 0.23) dex and (0.41 ± 0.28) dex, with a mean value of 0.19 dex and 1$\sigma$ dispersion as 0.26 dex. The largest mean offset of (0.41 ± 0.28) dex comes from the mean offset between the $M_{\text{BH}}$ estimated with the Mg $\text{ii}$ line-based calibration (Kollmeier et al. 2006) and the reference $M_{\text{BH}}$. We suspect that the larger offsets may be due to the sample selection; the sample that Kollmeier et al. (2006) adopted covers relatively lower and narrower redshift (luminosity) ranges. The mean values of the offset distributions are also shown as the vertical dashed lines in Figure 6.

If only the offsets are considered, our Mg $\text{ii}$ based calibration show smaller offsets from the reference log $M_{\text{BH}}$, with the mean absolute offset value around $\sim$0.01 dex compared to the mean offset $\sim$0.19 dex for the earlier studies. However, after taking into account the relatively large 1$\sigma$ dispersions of these mean differences, our results generally agree with the calibrations of earlier studies.
Figure 4. $\log \text{FWHM}_{\text{MgII}}$ vs. $\log \text{FWHM}_{\beta}$. The red symbols refer to the quasars with spectra labeled as "median," the black ones represent the quasars labeled as "good." The green line denotes the 1:1 relation, while the black line refers to the fitting using the BCES method.

Figure 5. $\log L_{3000}$ vs. $\log L_{5100}$. The red dots refer to the quasars with spectra labeled as "median," while the black ones represent the quasars labeled as "good." The black line denotes the fitting using the BCES method.
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Figure 6. Distributions of the offsets between different FWHM_{Mg\,II} and L_{5100} based log \( M_{BH} \) and the reference log \( M_{BH} \) calculated based on the FWHM_{H\beta} and L_{5100} using the calibration from Vestergaard & Peterson (2006). The vertical dashed lines refer to the mean values of the offset distributions and the solid black line denotes the offset value at 0. The red histogram is the same in each panel.

Thanks to the available SDSS spectroscopy of the \( z \sim 3.5 \) quasars, we also estimate BH masses using the FWHM_{CIV} and \( L_{150} \) based calibration from Vestergaard & Peterson (2006). The measured BH masses are compared with the reference BH masses and the Mg\,II line-based \( M_{BH} \) estimates using Equation (2). They are generally consistent with each other, with mean offsets of 0.08 ± 0.36 dex and 0.10 ± 0.33 dex, respectively.

In all, with simultaneous observations of the Mg\,II and H\beta lines, we ensure the reliability to measure BH masses based on the Mg\,II line, without the influences of flux variability. Moreover, we get the consistent results with the earlier studies which implies that flux variability has marginal influence on BH mass measurements using the Mg\,II line compared to the H\beta-based BH mass estimates.

6.2. Black Hole Accretion and Growth

Reliable estimates of BH masses and Eddington ratios (\( R_{\text{edd}} = L_{\text{bol}} / L_{\text{edd}} \)) of our sample can be obtained based on their H\beta lines. Here the bolometric luminosity \( L_{\text{bol}} \) is calculated as \( f_{\lambda} L_{5100} \) and the bolometric correction factor \( f_{\lambda} \) is assumed to be 9.26 (Richards et al. 2006). This provides a good laboratory to investigate the BH growth for quasars at \( z \sim 3.5 \).

For the 20 quasars labeled as “good” with full H\beta coverage, the minimum and maximum \( R_{\text{edd}} \) values are \( \sim 0.30 \pm 0.01 \) and \( 3.05 \pm 0.25 \), respectively. The median value is 1.12 with 1 \( \sigma \) scatter of 0.79. This indicates that these quasars are accreting at high \( R_{\text{edd}} \) at this redshift (and luminosity) range. From the log \( R_{\text{edd}} \) measurements and their uncertainties shown in Column 9 of Table 2, we notice that \( R_{\text{edd}} \) of five quasars are above unity with 3\( \sigma \) significance. If the typical systematic uncertainty of RM-based \( M_{BH} \) estimates as 0.3–0.4 dex (Vestergaard 2002; Onken et al. 2004; Peterson et al. 2004) is considered, the \( R_{\text{edd}} \) values of all the quasars are consistent with unity within three times their measurement uncertainties.

To investigate the BH growth time for the high redshift luminous quasars, we assume that the quasars are accreting at a constant \( R_{\text{edd}} \) as listed in Table 2. Then the growth time can be described similar to Netzer et al. (2007):

\[
\tau_{\text{growth}} = 0.38 \, \text{Gyr} \frac{\eta/(1-\eta)}{f_{\lambda} L_{5100} / L_{\text{edd}}} \log \frac{M_{BH}}{M_{\text{seed}}} \frac{1}{f_{\text{active}}},
\]

where the accretion efficiency \( \eta \) is assumed to be 0.1 and \( f_{\text{active}} \) is the duty cycle of quasar activity, i.e., fraction of time when a BH is active.

According to the current paradigm, the BH growth is due to accretion of surrounding gas onto much smaller initial seeds. BH seeds with tens to hundreds of \( M_{\odot} \) and those with \( 10^{4} \) to \( 10^{6} \) \( M_{\odot} \) can be traced back to the first generation stars (Bromm et al. 1999) and direct collapse of supermassive objects (Begelman et al. 2006), respectively.

With \( f_{\text{active}} \) of 1 and \( M_{\text{seed}} \) of \( 10^{4} \, M_{\odot} \), all the quasars in our sample can grow to their estimated BH masses within the age of the universe at their corresponding redshifts. Compared to the \( 2.2 < z < 3.4 \) quasars with \( 10^{45.2} \text{erg s}^{-1} < L_{5100} < 10^{46.4} \text{erg s}^{-1} \) in Netzer et al. (2007), under the same settings of \( f_{\text{active}} \) and \( M_{\text{seed}} \), only 27% of their 15 sources have enough time to grow their BH masses. For the quasars having not enough
time to grow their BH masses at $z < 3$, Netzer et al. (2007) suggested that they may have gone through one or more past episodes with high accretion rates than the estimated values; the BH growth of the $z \sim 3.5$ quasars in our sample seem to fit the scenario. Of course, our quasars are not likely from the same progenitor population of the quasars at $z < 3$ studied in Netzer et al. (2007), because at the observed accretion rates, the quasars in our sample already have larger BH masses than the quasars in their sample.

As our sample is more luminous ($10^{46.6} \text{ erg s}^{-1} < L_{5100} < 10^{47.5} \text{ erg s}^{-1}$) with higher accretion rates, given the simple BH growth model, it is not surprising to find that a larger fraction of quasars fits the growth scenarios at the same $f_{\text{active}}$ and $M_{\text{seed}}$. To investigate whether or not the systematic uncertainty of $M_{\text{BH}}$ estimates influence the conclusion, we adopt a Monte-Carlo method to resample the BH mass of each quasar in our sample according to the assumed BH mass distribution; for each quasar the distribution of $\log M_{\text{BH}}$ is a Gaussian with a peak at its $\log M_{\text{BH}}$ value shown in Column 6 of Table 2 and a dispersion of 0.3 dex (the typical systematic uncertainty of RM-based $M_{\text{BH}}$ estimates). This process is iterated 50 times to generate 50 different mock samples with the same number of quasars as our sample. We find that the conclusion is not influenced by the systematic uncertainties of $M_{\text{BH}}$ estimates; a larger fraction of quasars in our sample fit the growth scenario at the same $f_{\text{active}}$ and $M_{\text{seed}}$ than the sample in Netzer et al. (2007).

7. CONCLUSION

In this paper we have empirically determined the relations between single epoch virial BH mass estimates based on different lines for 21 high redshift luminous quasars ($3.2 < z < 3.9$, $L_{5100} > 10^{46.6} \text{ erg s}^{-1}$), using high-quality near-IR spectroscopy. Our sample has negligible contamination from host galaxy, and is relatively large enough to obtain some statistically significant results for the sample.

The main conclusions are as follows.

1. The Mg\textsc{ii} FWHM is well correlated with the H$\beta$ FWHM, confirming itself as a good substitute for $FWHM_{H\beta}$ in the BH mass estimates.
2. The continuum luminosity at 5100 Å correlates well with the continuum luminosity at 3000 Å and broad emission line luminosities (H$\beta$ and Mg\textsc{ii}).
3. With simultaneous near-IR spectroscopy of the H$\beta$ and Mg\textsc{ii} lines, we ensure the reliability to estimate BH masses based on the Mg\textsc{ii} line for high redshift quasars, without the influences of flux variability.
4. With the reliable H$\beta$ line based BH mass and Eddington ratio estimates, we find $1.90 \times 10^9 M_\odot \lesssim M_{\text{BH}} \lesssim 1.37 \times 10^{10} M_\odot$ with a median of $\sim 5.14 \times 10^9 M_\odot$. We also find that the $z \sim 3.5$ quasars in our sample are accreting at Eddington ratios in the range from 0.30 to 3.05, with a median value of $\sim 1.12$.
5. With a duty cycle of 1 and a seed BH mass at $10^4 M_\odot$, the quasars in this $z \sim 3.5$ sample can grow to their estimated BH masses within the age of the universe at their redshifts, under their high accretion rates.

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