Discrete Memoryless Interference and Broadcast Channels with Confidential Messages: Secrecy Rate Regions

Ruoheng Liu, Member, IEEE, Ivana Marić, Member, IEEE, Predrag Spasojević, Member, IEEE, and Roy D. Yates Member, IEEE

Abstract—We study information-theoretic security for discrete memoryless interference and broadcast channels with independent confidential messages sent to two receivers. Confidential messages are transmitted to their respective receivers with information-theoretic secrecy. That is, each receiver is kept in total ignorance with respect to the message intended for the other receiver. The secrecy level is measured by the equivocation rate at the eavesdropping receiver. In this paper, we present inner and outer bounds on secrecy capacity regions for these two communication systems. The derived outer bounds have an identical mutual information expression that applies to both channel models. The difference is in the input distributions over which the expression is optimized. The inner bound rate regions are achieved by random binning techniques. For the broadcast channel, a double-binning coding scheme allows for both joint encoding and preserving of confidentiality. Furthermore, we show that, for a special case of the interference channel, referred to as the switch channel, the two bound bounds meet. Finally, we describe several transmission schemes for Gaussian interference channels and derive their achievable rate regions while ensuring mutual information-theoretic secrecy. An encoding scheme in which transmitters dedicate some of their power to create artificial noise is proposed and shown to outperform both time-sharing and simple multiplexed transmission of the confidential messages.

I. INTRODUCTION

The broadcast nature of a wireless medium allows for the transmitted signal to be received by all users within the communication range. Hence, wireless communication sessions are very susceptible to eavesdropping. The information-theoretic single user secure communication problem was first characterized using the wiretap channel model proposed by Wyner [1]. In this model, a single source-destination communication link is eavesdropped by a wiretapper via a degraded channel. The secrecy level is measured by the equivocation rate at the wiretapper. Wyner showed that secure communication is possible without sharing a secret key between legitimate users, and determined the tradeoff between the transmission rate and the secrecy level [1]. This result was generalized by Csiszár and Körner who determined the capacity region of the broadcast channel with confidential messages [2] in which a message intended for one of the receivers is confidential.

Following the work of Wyner [1] and Csiszár and Körner [2], the more recent information-theoretic research on secure communication focuses at implementing security on the physical layer. Based on independent efforts, the authors of [3] and [4] described achievable secure rate regions and outer bounds for a two-user discrete memoryless multiple access channel with confidential messages. This model generalizes the multiple access channel (MAC) [5, Sec. 14.3] by allowing each user (or one of the users) to receive noisy channel outputs and, hence, to eavesdrop the confidential information sent by the other user. In addition, the Gaussian MAC wiretap channel has been analyzed in [6]–[10]. The relay channel with confidential messages where the relay node acts as both a helper and a wiretapper has been considered in [11]. The relay-eavesdropper channel has been proposed in [12]. More recently, the cognitive interference channel with confidential messages has been addressed in [13]. The effects of fading on secure wireless communication have been studied in [14]–[18].

In this paper, we study two distinct but related in multi-terminal secure communication problems following the information-theoretic approach. We focus on discrete memoryless interference and broadcast channels with independent confidential messages sent to two receivers. Confidential messages are transmitted to their respective receivers while ensuring mutual information-theoretic secrecy. That is, each receiver is kept in total ignorance with respect to the message intended for the other receiver. We first derive outer bounds on capacity regions for these two communication systems. These bounds have an identical mutual information expression. The expression is optimized over different input distributions, i.e., for the interference channel, the two senders offer independent inputs to the channel and, for the broadcast channel, the sender jointly encodes both messages. We also derive achievable rate regions for the two channel models. Here, we only consider sending confidential messages and, hence, no common message in the sense of Marton [19] is conveyed to the receivers in the case of the broadcast channel. The inner bounds are achieved using random binning techniques. For the broadcast channel, a double-binning coding scheme which allows for
both joint precoding as in the classical broadcast channel [19], and preserving of confidentiality. Similarly, ensuring of confidential messages precludes partial decoding of the message intended for the other receiver in the case of the interference channel. Hence, rate-splitting encoding used by Carleial [20] and Han and Kobayashi [21] employed with the classical interference channel is precluded. Instead, the encoders will use only stochastic encoders. We show that for the special case of the interference channel, referred to as the switch channel, derived bounds meet. Finally, we describe several transmission schemes for general Gaussian interference channels and derive their achievable rate regions while still ensuring information-theoretic secrecy. An encoding scheme in which transmitters dedicate some of their power to create artificial noise is proposed and shown to outperform both time-sharing and simple multiplexed transmission of the confidential messages.

The remainder of this paper is organized as follows. The notation and the channel model are given in Sec. II. We state the main results in Sec. III. Outer bounds are derived in Sec. IV. Inner bounds associated with the achievable coding scheme for the interference and broadcast channels with confidential messages are summarized in Sec. V. Finally, the results are summarized in Sec. VI.

II. DEFINITIONS AND NOTATIONS

A. Notations

Throughout the paper, a random variable is denoted with an upper case letter (e.g., $X$), its realization is denoted with the corresponding lower case letter (e.g., $x$), the finite alphabet of the random variable is denoted with the corresponding calligraphic letter (e.g., $\mathcal{X}$), and its probability distribution is denoted with $P_X(x)$. For example, the random variable $X$ with probability distribution $P_X(x) = P_X(x)$ takes on values in the finite alphabet $\mathcal{X}$. A boldface symbol denotes a sequence with the following conventions

$$X = [X_1, \ldots, X_n], \quad X^i = [X_1, \ldots, X_i],$$

and

$$X^{i} = [X_i, \ldots, X_n].$$

Finally, we use $A(e^{(n)}(P_X))$ to denote the set of (weakly) jointly typical sequences $x$ with respect to $P(x)$ (see [5] for more details).

B. The Interference Channel with Confidential Messages

Consider a discrete memoryless interference channel with finite input alphabets $\mathcal{X}_1, \mathcal{X}_2$, finite output alphabets $\mathcal{Y}_1, \mathcal{Y}_2$, and the channel transition probability distribution $P(y_1, y_2|x_1, x_2)$. Two transmitters wish to send independent, confidential messages to their respective receivers. We refer to such a channel as the interference channel with confidential messages (IC-CM). This communication model is shown in Fig. 1. Symbols $(x_1, x_2) \in (\mathcal{X}_1 \times \mathcal{X}_2)$ are the channel inputs at transmitters 1 and 2, and $(y_1, y_2) \in (\mathcal{Y}_1 \times \mathcal{Y}_2)$ are the channel outputs at receivers 1 and 2, respectively.

Transmitter $t$, $t = 1, 2$, intends to send an independent message $W_t \in \{1, \ldots, M_t\}$ to the desired receiver $t$ in $n$ channel uses while ensuring information-theoretic secrecy. The channel is memoryless in the sense that

$$P(y_1, y_2|x_1, x_2) = \prod_{i=1}^{n} P(y_{1,i}, y_{2,i}|x_{1,i}, x_{2,i}).$$

A stochastic encoder for transmitter $t$ is described by a matrix of conditional probabilities $f_t(x_i|w_i)$, where $x_i \in \mathcal{X}_i$, $w_i \in \mathcal{W}_i$, and

$$\sum_{x_i \in \mathcal{X}_i} f_t(x_i|w_i) = 1.$$

Decoding functions are mappings $\psi_t : \mathcal{Y}_t \rightarrow \mathcal{W}_t$. Secrecy levels at receivers 1 and 2 are measured with respect to the equivocation rates

$$\frac{1}{n} H(W_2|Y_1) \quad \text{and} \quad \frac{1}{n} H(W_1|Y_2).$$

(1)

An $(M_1, M_2, n, P^{(n)}_c)$ code for the interference channel consists of two encoding functions $f_1$, $f_2$, two decoding functions $\psi_1$, $\psi_2$, and the corresponding maximum average error probability

$$P^{(n)}_c \triangleq \max\{P^{(n)}_{c,1}, P^{(n)}_{c,2}\}$$

(2)

where, for $t = 1, 2$,

$$P^{(n)}_{c,t} = \sum_{w_1, w_2} \frac{1}{M_1 M_2} P[\psi_t(Y_t) \neq w_t|(w_1, w_2) \text{ sent}].$$

A rate pair $(R_1, R_2)$ is said to be achievable for the interference channel with confidential messages if, for any $\epsilon_0 > 0$, there exists a $(M_1, M_2, n, P^{(n)}_c)$ code such that

$$M_t \geq 2^{nR_t} \quad \text{for } t = 1, 2$$

and the reliability requirement

$$P^{(n)}_c \leq \epsilon_0$$

(4)

and the security constraints

$$nR_1 - H(W_1|Y_2) \leq n\epsilon_0$$

(5a)

$$nR_2 - H(W_2|Y_1) \leq n\epsilon_0$$

(5b)

are satisfied. This definition corresponds to the so-called weak secrecy-key rate [22]. A stronger measurement of the secrecy level has been defined by Maurer and Wolf in terms of the absolute equivocation [22], where the authors have shown that the former definition could be replaced by the latter without any rate penalty for the wiretap channel.

The capacity region of the IC-CM is the closure of the set of all achievable rate pairs $(R_1, R_2)$, denoted by $\mathcal{C}_{IC}$. 
Coding function at the receiver

Decoding functions

Messages are measured, respectively, at receivers 1 and 2 in terms of \( f \) as given by (5a) and (5b). The channel is memoryless in the \( n \) channel uses while ensuring information-theoretic secrecy as given by (5a) and (5b). The channel is memoryless in the sense that

\[
P(y_1, y_2|x) = \prod_{i=1}^{n} P(y_{1,i}, y_{2,i}|x_i).
\]

A stochastic encoder is specified by a matrix of conditional probabilities \( f(x|w_1, w_2) \), where \( x \in \mathcal{X}^n \), \( w_i \in \mathcal{W}_i \), and

\[
\sum_{x \in \mathcal{X}^n} f(x|w_1, w_2) = 1.
\]

Note that \( f(x|w_1, w_2) \) is the probability that the pair of messages \((w_1, w_2)\) are encoded as the channel input \( x \). The decoding function at the receiver \( t \) is a mapping \( \phi_t : \mathcal{Y}_t \rightarrow \mathcal{W}_t \).

The secrecy levels of confidential messages \( \mathcal{W}_2 \) and \( \mathcal{W}_1 \) are measured, respectively, at receivers 1 and 2 in terms of the equivocation rates (1). An \((M_1, M_2, n, P_e^{(n)})\) code for the broadcast channel consists of the encoding function \( f \), decoding functions \( \phi_1, \phi_2 \), and the maximum error probability \( P_e^{(n)} \) in (2), where, for \( t = 1, 2 \),

\[
P_e^{(n)} = \sum_{w_1, w_2} \frac{1}{M_1 M_2} P[\phi_t(Y_t) \neq w_t|w_1, w_2 \text{ sent}].
\]

A rate pair \((R_1, R_2)\) is said to be achievable for the broadcast channel with confidential messages if, for any \( \epsilon_0 > 0 \), there exists a \((M_1, M_2, n, P_e^{(n)})\) code which satisfies (3)–(5).

The capacity region of the BC-CM is the set of all achievable rate pairs \((R_1, R_2)\), denoted by \( C_{BC} \).

Finally, we propose several transmission schemes for Gaussian interference channels and derive their achievable rate regions under information-theoretic secrecy.

A. Interference Channel with Confidential Messages

Let \( U, V_1, \) and \( V_2 \) be auxiliary random variables. We consider the following two classes of joint distributions for the interference channel. Let \( \pi_{IC-O} \) be the class of distributions \( P(u, v_1, v_2, x_1, x_2, y_1, y_2) \) that factor as

\[
P(u)P(v_1, v_2|u)P(x_1|v_1)P(x_2|v_2)P(y_1, y_2|x_1, x_2),
\]

and \( \pi_{IC-1} \) be the class of distributions that factor as

\[
P(u)P(v_1|u)P(v_2|u)P(x_1|v_1)P(x_2|v_2)P(y_1, y_2|x_1, x_2).
\]

**Theorem 1:** [Outer bound for IC-CM] Let \( \mathcal{R}_O(\pi_{IC-O}) \) denote the union of all \((R_1, R_2)\) satisfying

\[
0 \leq R_1 \leq \min \left[ I(V_1; Y_1|U) - I(V_1; Y_2|V_2, U), \right.
\]

\[
0 \leq R_2 \leq \min \left[ I(V_2; Y_2|U) - I(V_2; Y_1|V_1, U), \right.
\]

over all distributions \( P(u, v_1, v_2, x_1, x_2, y_1, y_2) \) in \( \pi_{IC-O} \). For the interference channel \((\mathcal{X}_1 \times \mathcal{X}_2, P(y_1, y_2|x_1, x_2), \mathcal{Y}_1 \times \mathcal{Y}_2)\) with confidential messages, the capacity region

\[
C_{IC} \subseteq \mathcal{R}_O(\pi_{IC-O}).
\]

**Proof:** We provide the proof of Theorem 1 in Sec. IV.

**Theorem 2:** [Inner bound for IC-CM] Let \( \mathcal{R}_{IC}(\pi_{IC-1}) \) denote the union of all \((R_1, R_2)\) satisfying

\[
0 \leq R_1 \leq I(V_1; Y_1|U) - I(V_1; Y_2|V_2, U)
\]

\[
0 \leq R_2 \leq I(V_2; Y_2|U) - I(V_2; Y_1|V_1, U)
\]

over all distributions \( P(u, v_1, v_2, x_1, x_2, y_1, y_2) \) in \( \pi_{IC-1} \). Any rate pair

\[
(R_1, R_2) \in \mathcal{R}_{IC}(\pi_{IC-1})
\]

is achievable for the interference channel with confidential messages.

**Proof:** We provide the proof in Sec. V.

To derive the achievable rate region for the IC-CM, we employ an auxiliary random variable \( U \) in the sense of Han-Kobayashi [21]. For a given \( U \), we consider two independent stochastic encoders, that is, the pre-coding auxiliary random variables \( V_1 \) and \( V_2 \) will be independent for a given \( U \), as given by (8). To ensure information-theoretic secrecy, the achievable rate \( R_1 \) includes a penalty term \( I(V_1; Y_2|V_2, U) \), which is a conditional mutual information of the receiver 2’s eavesdropper channel while assuming the receiver 2 can first decode its own information.

B. Broadcast Channel with Confidential Messages

For the broadcast channel, we focus on the class of distributions \( P(u, v_1, v_2, x, y_1, y_2) \) that factor as

\[
P(u)P(v_1, v_2|u)P(x|v_1, v_2)P(y_1, y_2|x).
\]

We refer to this class as \( \pi_{BC} \).
**Theorem 3:** [outer bound for BC-CM] Let $\mathbb{R}_O(\pi_{BC})$ denote the union of all $(R_1, R_2)$ satisfying

$$R_1 \geq 0, \ R_2 \geq 0$$
$$R_1 \leq \min \left[ \frac{I(V_1; Y_1 | U) - I(V_1; Y_2 | U)}{I(V_1; Y_2 | U) - I(V_1; V_2 | U)} \right] \quad (12a)$$
$$R_2 \leq \min \left[ \frac{I(V_2; Y_2 | U) - I(V_2; Y_1 | U)}{I(V_2; Y_1 | U) - I(V_2; V_1 | U)} \right] \quad (12b)$$

over all distributions $P(u, v_1, v_2, x, y_1, y_2)$ in $\pi_{BC}$ and auxiliary random variables $U$, $V_1$, and $V_2$ satisfying $U \rightarrow V_1 \rightarrow X$ and $U \rightarrow V_2 \rightarrow X$. (13)

For the broadcast channel $(X, P(y_1, y_2|x), Y_1 \times Y_2)$ with confidential messages, the capacity region

$$\mathcal{C}_{BC} \subseteq \mathbb{R}_O(\pi_{BC}).$$

**Proof:** We provide the proof of Theorem 3 in Sec. IV.

**Remark 1:** Outer bounds for the BC-CM and the IC-CM have a same mutual information expression $\mathbb{R}_O(\cdot)$, but, they are optimized over different input distributions $\pi_{BC}$ and $\pi_{IC-O}$, respectively.

**Theorem 4:** [inner bound for BC-CM] Let $\mathbb{R}_{BC}(\pi_{BC})$ denote the union of all $(R_1, R_2)$ satisfying

$$R_1 \geq 0, \ R_2 \geq 0$$
$$R_1 \leq I(V_1; Y_1 | U) - I(V_1; V_2 | U) - I(V_1; Y_2 | V_2 | U) \quad (14a)$$
$$R_2 \leq I(V_2; Y_2 | U) - I(V_2; V_1 | U) - I(V_2; Y_1 | V_1 | U) \quad (14b)$$

over all distributions $P(u, v_1, v_2, x, y_1, y_2)$ in $\pi_{BC}$. Any rate pair

$$(R_1, R_2) \in \mathbb{R}_{BC}(\pi_{BC})$$

is achievable for the broadcast channel with confidential messages.

**Proof:** We provide the proof in Sec. V-B.

We note that, for a broadcast channel, we can employ joint encoding at the transmitter. Hence, the achievable coding scheme for the BC-CM is based on the double-binning scheme which combines the Gel’fand-Pinsker binning [23] and the random binning. To preserve confidentiality, the achievability bounds on $R_1$ and $R_2$ each include the penalty term $I(V_1; V_2 | U)$. Without the confidentiality constraint, Marton’s inner bound [19] on the broadcast channel illustrates only that the sum rate has the penalty term $I(V_1; V_2 | U)$. To ensure information-theoretic secrecy, the proposed coding scheme pays “double” when jointly encoding at the transmitter.

**Example 1:** [less noisy broadcast channel] Consider a special class of broadcast channels in which the channel $X \rightarrow Y_1$ is less noisy than the channel $X \rightarrow Y_2$, i.e.,

$$I(V; Y_1) \geq I(V; Y_2) \quad (15)$$

for every $V \rightarrow X \rightarrow (Y_1, Y_2)$ [2]. We first consider the outer bound of the less noisy BC-CM. Based on the Markov chains in (13) and the definition (15), we have

$$I(V_1; Y_1 | U = u) \geq I(V_1; Y_2 | U = u)$$
$$I(V_2; Y_1 | U = u) \geq I(V_2; Y_2 | U = u),$$

which implies that

$$I(V_1; Y_1 | U) \geq I(V_1; Y_2 | U)$$
$$I(V_2; Y_1 | U) \geq I(V_2; Y_2 | U).$$

Hence the outer bound can be rewritten as the union of all $(R_1, R_2)$ satisfying

$$R_1 \leq \max [I(X; Y_1) - I(X; Y_2)] \quad (16a)$$
$$R_2 = 0 \quad (16b)$$

where (16a) follows from [2, Theorem 3]. Next, by applying Theorem 4 and setting $V_2 = U = \text{const}$, we obtain the identical rate region as (16). This result implies that only the “better” user can get the non-zero secrecy rate for the less noisy BC-CM. Note that, the single-antenna Gaussian broadcast channel is a special case of the less noisy broadcast channel.

In the following, we consider a sufficient condition under which both $R_1$ and $R_2$ can be strictly positive for the BC-CM.

**Corollary 1:** For a broadcast channel, if there exist a distribution $P(u, v_1, v_2, x, y_1, y_2) \in \pi_{BC}$ for which

$$I(V_1; Y_1 | U) > I(V_1; V_2 | U) \quad (17a)$$
$$I(V_2; Y_2 | U) > I(V_2; Y_1 | U), \quad (17b)$$

then both receivers can achieve strictly positive rates while ensuring information-theoretic secrecy.

**Proof:** The result is obtained by applying Theorem 4 and by setting $R_1 > 0$ and $R_2 > 0$.

More recently, motivated by this work, the multiple-antenna Gaussian broadcast channel with confidential messages was studied in [24]. It was shown that with multiple antennas at transmitters, strictly positive rates to both receivers can be achieved while ensuring information-theoretic secrecy.

**C. Switch Channel**

In this subsection, we obtain the secrecy capacity region for a special case of the interference channel referred to as the switch channel (SC). As shown in Fig. 3 receivers in the SC cannot listen to both transmissions (from encoders 1 and 2) at the same time. For example, each encoder may transmit at a different frequency, while each receiver may listen only to one frequency during each symbol time $i$. We assume that each receiver $i \in \{1, 2\}$ has a random switch $s_i \in \{1, 2\}$, which chooses between $t$ and $\bar{t}$ independently at each symbol time $i$ with probabilities

$$P(S_{t,i} = t) = \tau_t$$
$$P(S_{\bar{t},i} = \bar{t}) = 1 - \tau_t, \ i = 1, \ldots, n$$

where $\bar{t}$ is the complement of $t$. Therefore, receiver $i$ listens to its own information $x_{t,i}$ from encoder $t$ whenever $S_{t,i} = t$, while it eavesdrops the signal $x_{\bar{t},i}$ when $S_{t,i} = \bar{t}$. By assuming that the switch state information is available at the receiver, we have that

$$P(y_{t,i} | x_{1,i}, x_{2,i}, s_{t,i}) = P(y_{t,i} | x_{1,i}) I(s_{t,i} = 1)$$
$$+ P(y_{t,i} | x_{2,i}) I(s_{t,i} = 2)$$
$$= P(y_{t,i} | x_{s_{t,i}}) \quad (18)$$
where $\mathbbm{1}(\cdot)$ is the indicator function.

The switch state information $\{S_{t,i}\}_{i=1}^{n}$ is an i.i.d. process known at receiver $t$. Hence, we can consider $s_{t,i}$ as part of the channel output, i.e., we set

$$y_{t,i} \triangleq \{z_{t,i}, s_{t,i}\}$$

where $z_{t,i}$ represents the received signal value at receiver $t$. Under this setting, we have the following theorem on the secrecy capacity region $\mathbb{C}_{SC}$ of SC-CM.

**Theorem 5:** For the switch channel with confidential messages, the capacity region $\mathbb{C}_{SC}$ is the union of all $(R_1, R_2)$ satisfying

\[ 0 \leq R_1 \leq I(V_1; Y_1|U) - I(V_1; Y_2|V_2, U) \]
\[ 0 \leq R_2 \leq I(V_2; Y_2|U) - I(V_2; Y_1|V_1, U) \]

over all distributions $P(u, v_1, v_2, x_1, x_2, y_1, y_2)$ in $\pi_{1C-1}$.

**Proof:** We provide the proof in the Appendix. □

**Remark 2:** In SC-CM, receiver $t$ listens to the desired information during time fraction $\tau_1$ and intercepts the other message during the time fraction $(1 - \tau_1)$. When $\tau_1 = \tau_2 = 1$, both receivers only listen to their own messages and thus SC-CM reduces to two independent parallel channels without the secrecy constraints. When $\tau_1 = 1$ and $\tau_2 = 0$, receiver 2 acts as an eavesdropper only and both $Y_1$ and $Y_2$ are independent with respect to the message $W_2$. Hence, in this case, SC-CM reduces to the wiretap channel [1].

**Example 2:** [noiseless memoryless switch channel] We assume that the channel is discrete memoryless and that the input-output relationship at each time instant satisfies

$$Y_{t,i} = \begin{cases} X_{1,i}, & S_{t,i} = 1 \\ X_{2,i}, & S_{t,i} = 2 \end{cases} \quad \text{for } i = 1, \ldots, n$$

where $P(S_{t,i} = t) = \tau_t$ and $\tau_1 + \tau_2 \geq 1$. Theorem 5 implies that the secrecy capacity region of this channel is:

$$\begin{align*}
(R_1, R_2) : & \quad R_1 \leq (\tau_1 + \tau_2 - 1)H(X_1) \\
& \quad R_2 \leq (\tau_1 + \tau_2 - 1)H(X_2)
\end{align*}$$

(22)

We note that here $\tau_1 + \tau_2 - 1$ equals $\tau_1 - (1 - \tau_2)$, the time that user 1 sends without user 2 listening and also equals $\tau_2 - (1 - \tau_1)$, the time that user 2 sends without user 1 listening.

**D. Gaussian Interference Channel with Confidential Messages**

We next consider a Gaussian interference channel (GIC) with confidential messages (GIC-CM) where each node employs a single antenna as shown in Fig. 4. We have proposed this problem originally in [25].

We assume the channel input and output symbols to be from an alphabet of real numbers. Following the standard form GIC [20], the received symbols are

\[ Y_1 = X_1 + \alpha_1 X_2 + N_1 \]
\[ Y_2 = \alpha_2 X_1 + X_2 + N_2 \]

where $\alpha_1$ and $\alpha_2$ are normalized crossover channel gains, $X_1$ and $X_2$ are transmitted symbols from encoders 1 and 2 with the average power constraint

$$\sum_{i=1}^{n} \frac{E[X_{i,t}^2]}{n} \leq P_t, \quad \text{for } t = 1, 2,$$

and $N_1$ and $N_2$ correspond to two independent, zero-mean, unit-variance, Gaussian noise variables. In the following, we focus on the *weak* interference channel, i.e., $0 \leq \alpha_1^2 < 1$ and $0 \leq \alpha_2^2 < 1$. We describe three transmission schemes and their achievable rate regions under the requirement of information-theoretic secrecy.

1) **Time-Sharing:** The transmission period is divided into two non-overlapping slots with time fractions $\rho_1$ and $\rho_2$, where $\rho_1 \geq 0$, $\rho_2 \geq 0$, and $\rho_1 + \rho_2 = 1$. Transmitter 1 sends confidential message $W_1$ in slot $t$ with time fraction $\rho_t$, $t = 1, 2$. We refer to this technique as the time-sharing scheme. We note that, in each slot, the channel reduces to a Gaussian wiretap channel [26]. Let $R_{GIC}^{[T]}$ denote the set of $(R_1, R_2)$ satisfying

\[ 0 \leq R_1 \leq \frac{\rho_1}{2} \left[ \log \left( 1 + \frac{P_1}{\rho_1} \right) - \log \left( 1 + \frac{\alpha_1^2 P_1}{\rho_1} \right) \right] \]
\[ 0 \leq R_2 \leq \frac{\rho_2}{2} \left[ \log \left( 1 + \frac{P_2}{\rho_2} \right) - \log \left( 1 + \frac{\alpha_2^2 P_2}{\rho_2} \right) \right] \]

over all time fractions $(\rho_1, \rho_2)$ pairs. Following [26], we can show that any rate pair

$$(R_1, R_2) \in R_{GIC}^{[T]}$$

is achievable for GIC-CM.

2) **Multiplexed Transmission:** In the multiplexed transmission scheme, we allow communication links to share the same degrees of freedom. Since we require information-theoretic secrecy for confidential messages, no partial decoding of the other transmitter’s message is allowed at a receiver. Hence, the interference results in an increase of the noise floor. Let

$$0 \leq \beta_t \leq 1, \quad t = 1, 2.$$
By independently choosing 
\[ V_t = X_t \sim \mathcal{N}[0, \beta_t P_t], \quad t = 1, 2 \]
and letting \( U \) serve as a convex combination operator, Theorem 2 implies that any rate pair 
\[ (R_1, R_2) \in \mathbb{R}^{[M]}_{\text{GIC}} \]
is achievable for GIC-CM, where \( \mathbb{R}^{[M]}_{\text{GIC}} \) denotes the convex hull of the set of \((R_1, R_2)\) satisfying
\[
R_1 \geq 0, \quad R_2 \geq 0
\]
\[
R_1 \leq \frac{1}{2} \log \left( 1 + \frac{\beta_1 P_1}{1 + \alpha_1^2 \beta_2 P_2} \right) - \frac{1}{2} \log(1 + \alpha_2^2 \beta_1 P_1)
\]
\[
R_2 \leq \frac{1}{2} \log \left( 1 + \frac{\beta_2 P_2}{1 + \alpha_2^2 \beta_1 P_1} \right) - \frac{1}{2} \log(1 + \alpha_1^2 \beta_2 P_2)
\]
over all power-control parameters \( \beta_1 \) and \( \beta_2 \).

3) Artificial Noise: We next describe a scheme which allows one of the transmitters (e.g., transmitter 2) to generate artificial noise. This strategy involves splitting of the transmission power of transmitter 2 into two parts \( P_{2,M} \) and \( P_{2,A} \), where
\[
P_{2,M} = (1 - \lambda) \beta_2 P_2, \quad P_{2,A} = \lambda \beta_2 P_2, \quad \text{and} \quad 0 \leq \lambda \leq 1,
\]
so that transmitter 2 encodes the confidential message with power \( P_{2,M} \) and generates artificial noise with power \( P_{2,A} \). The artificial noise can spoil the received signal of receiver 2 and, hence, protect the confidential message of transmitter 1. In this sense, this scheme allows transmitter cooperation without exchanging confidential messages. Let \( U \) serve as a convex combination operator,
\[
X_1 = V_1 \quad \text{and} \quad X_2 = V_2 + A_2 \quad (26)
\]
where \( V_1, V_2, \) and \( A_2 \) are independent Gaussian random variables:
\[
V_1 \sim \mathcal{N}[0, \beta_1 P_1], \quad V_2 \sim \mathcal{N}[0, P_{2,M}], \quad \text{and} \quad A_2 \sim \mathcal{N}[0, P_{2,A}].
\]
Here \( A_2 \) denotes the artificial noise which cannot be predicted and subtracted by either receiver. Since
\[
Y_1 = X_1 + \alpha_1 X_2 + N_1 = V_1 + \alpha_1 (V_2 + A_2) + N_1
\]
and
\[
Y_2 = \alpha_2 X_1 + X_2 + N_1 = \alpha_2 V_1 + (V_2 + A_2) + N_2,
\]
we have
\[
I(V_1; Y_1) = I(V_1; V_1 + \alpha_1 (V_2 + A_2) + N_1) = h(V_1 + \alpha_1 (V_2 + A_2) + N_1) - h(\alpha_1 (V_2 + A_2) + N_1)
\]
\[
= \frac{1}{2} \log \left( 1 + \frac{\beta_1 P_1}{1 + \alpha_2 \beta_1 P_2} \right)
\]
and
\[
I(V_1; Y_2) = I(V_1; \alpha_2 V_1 + V_2 + A_2 + N_2 | V_2) = h(\alpha_2 V_1 + A_2 + N_2) - h(A_2 + N_2)
\]
\[
= \frac{1}{2} \log \left( 1 + \frac{\alpha_2 \beta_1 P_1}{1 + \alpha_2^2 \beta_2 P_2} \right).
\]

Similarly, we can calculate
\[
I(V_2; Y_1) = \frac{1}{2} \log \left( 1 + \frac{(1 - \lambda) \beta_2 P_2}{1 + \alpha^2 \beta_1 P_2} \right)
\]
and
\[
I(V_2; Y_2 | Y_1) = \frac{1}{2} \log \left( 1 + \frac{(1 - \lambda) \alpha^2 \beta_2 P_2}{1 + \alpha^2 \beta_2 P_2} \right).
\]

Applying Theorem 2, we can prove that any rate pair 
\[(R_1, R_2) \in \mathbb{R}^{[A]}_{\text{GIC}}\]
is achievable for GIC-CM, where \( \mathbb{R}^{[A]}_{\text{GIC}} \) denotes the convex hull of the set of \((R_1, R_2)\) satisfying
\[
0 \leq R_1 \leq \frac{1}{2} \log \left( 1 + \frac{\beta_1 P_1}{1 + \alpha_2 \beta_1 P_2} \right) - \frac{1}{2} \log(1 + \alpha_2 \beta_1 P_1)
\]
\[
0 \leq R_2 \leq \frac{1}{2} \log \left( 1 + \frac{(1 - \lambda) \beta_2 P_2}{1 + \alpha_2 \beta_2 P_2} \right) - \frac{1}{2} \log(1 + \alpha_2 \beta_2 P_2)
\]
over all power-control parameter pair \((\beta_1, \beta_2)\) and the power-splitting parameter \( \lambda \). Furthermore, the achievable region can be increased by reversing the roles of transmitters 1 and 2.

Remark 3: We note that secure communication in a Gaussian channel with two senders and two receivers was also considered in [9], [10] for the Gaussian MAC with a wiretapper (GMAC-WT). In this setting, both messages are to be conveyed to one of the receivers and none to the other receiver. Although the two problem formulations differ, the absence of rate splitting in the interference channel results in that the two proposed encoding schemes have a closer relationship than the schemes suggested for the classical MAC and interference channels. In fact, the encoding scheme proposed in [9], [10] for the GMAC-WT, referred to as cooperative jamming, and our encoding scheme which creates artificial noise in (26) are the same.

Example 3: In Fig. 5, we compare the achievable regions:
\[
\mathbb{R}^{[T]}_{\text{GIC}}, \mathbb{R}^{[M]}_{\text{GIC}}, \text{ and } \mathbb{R}^{[A]}_{\text{GIC}}
\]
by numerical calculation, for
\[
P_1 = P_2 = 10 \quad \text{and} \quad \alpha_1 = \alpha_2 = 0.2
\]
in Fig. 5a and
\[
P_1 = P_2 = 100 \quad \text{and} \quad \alpha_1 = \alpha_2 = 0.2
\]
in Fig. 5b. Both numerical results illustrate that the artificial noise strategy allows for communication over larger rates, when compared to the time-sharing and multiplexed transmission schemes.
Since and we can rewrite (30) as follows
\[ H(W_1|Y_2) \leq \epsilon_0 \log(M_1 - 1) + h(\epsilon_0) \triangleq n\delta_1. \] (28a)
\[ H(W_2|Y_2) \leq \epsilon_0 \log(M_2 - 1) + h(\epsilon_0) \triangleq n\delta_2. \] (28b)
where \( h(x) \) is the binary entropy function. On the other hand, the security constraint \( 5a \) implies that
\[ nR_1 = H(W_1) \leq H(W_1|Y_2) + n\epsilon_0. \] (29)
In fact, the bound \( 9 \) on \( R_1 \) is based on the following two different upper bounds on the equivocation \( H(W_1|Y_2) \).

A. First Bound
The first upper bound is derived by applying the techniques in [2]. By using Fano’s inequality \( 38 \), we obtain the following bound on the equivocation
\[ H(W_1|Y_2) \leq H(W_1|Y_2) - H(W_1|Y_1) + n\delta_1. \] (30)
Let
\[ U_i = (Y_1^{i-1}, Y_2^{i+1}). \] (31)
Since \((U_i, Y_{2,i}) = (Y_1^{i-1}, Y_2^{i+1}) = (U_{i-1}, Y_{1,i-1})\), we have
\[ H(W_1|U_i, Y_{2,i}) - H(W_1|U_{i-1}, Y_{1,i-1}) = 0 \]
and we can rewrite \( 30 \) as follows
\[ H(W_1|Y_2) \leq H(W_1|Y_2) - H(W_1|Y_1) + \sum_{i=2}^{n} [H(W_1|U_i, Y_{2,i}) - H(W_1|U_{i-1}, Y_{1,i-1})] + n\delta_1. \] (32)
Note that
\[ Y_1 = (U_n, Y_{1,n}) \quad \text{and} \quad Y_2 = (U_1, Y_{2,1}). \]
Hence, the bound \( 32 \) can be expressed as follows
\[ H(W_1|Y_2) \leq H(W_1|U_1, Y_{2,1}) - H(W_1|U_n, Y_{1,n}) + \sum_{i=2}^{n} H(W_1|U_i, Y_{2,i}) - H(W_1|U_{i-1}, Y_{1,i-1}) + n\delta_1. \]
(33)
Inequalities \( 29 \) and \( 33 \) imply that
\[ nR_1 - n(\delta_1 + \epsilon_0) \leq \sum_{i=1}^{n} [I(W_1; Y_{1,i}|U_i) - I(W_1; Y_{2,i}|U_i)]. \]
Now, for \( \delta \triangleq \delta_1 + \epsilon_0 \), we have
\[ R_1 \leq \frac{1}{n} \sum_{i=1}^{n} [I(W_1; Y_{1,i}|U_i) - I(W_1; Y_{2,i}|U_i)] + \delta. \] (34)

Following [5, Chapter 14], we introduce a random variable \( Q \) uniformly distributed over \( \{1, 2, \ldots, n\} \) and independent of \( (W_1, W_2, X_1, X_2, Y_1, Y_2) \). Now we can bound \( R_1 \) as follows
\[ R_1 \leq \frac{1}{n} \sum_{i=1}^{n} [I(W_1; Y_{1,i}|U_i, Q = i) - I(W_1; Y_{2,i}|U_i, Q = i)] + \delta. \]
(35)
Let
\[ U \triangleq (U_Q, Q), \quad X_1 \triangleq X_1, Q, \quad X_2 \triangleq X_2, Q, \]
\[ Y_1 \triangleq Y_1, Q, \quad Y_2 \triangleq Y_2, Q, \]
\[ V_1 \triangleq (W_1, U), \quad V_2 \triangleq (W_2, U). \] \tag{36}

Note that, under the setting of (36), the conditional distribution of \( P(y_1, y_2|x_1, x_2) \) coincides with the original channel transition probability. We can rewrite (35) as
\[ R_1 \leq I(V_1; Y_1 | U) - I(V_1; Y_2 | U) + \delta. \] \tag{37}

Remark 4: Note that we employ only Fano’s inequality \((28a)\) to derive the first bound on \(R_1\).

B. Second Bound

The basic idea of the second bound can be described as follows. We assume that a genie gives receiver 1 message \(W_2\), while receiver 2 attempts to evaluate the equivocation with \(W_2\) as side information.

Now, the equivocation can be upper bounded by
\[ H(W_1 | Y_2) \leq H(W_1, W_2 | Y_2) = H(W_1 | Y_2, W_2) + H(W_2 | Y_2). \] \tag{38}

By applying (28a) and (28b), we have
\[ H(W_1 | Y_1) \leq n\delta_1 \quad \text{and} \quad H(W_2 | Y_2) \leq n\delta_2. \] \tag{39}

Since \( H(W_1 | Y_1, W_2) \leq H(W_1 | Y_1) \), we can further bound (38) as follows
\[ H(W_1 | Y_2) \leq H(W_1 | Y_2, W_2) + n\delta_2 \leq H(W_1 | Y_2, W_2) - H(W_1 | Y_1, W_2) + n(\delta_1 + \delta_2). \] \tag{40}

Let \( \delta' = \delta_1 + \delta_2 + \epsilon_0 \). Following the same approach as in (30)–(36), we obtain
\[ R_1 \leq I(V_1; Y_1 | V_2, U) - I(V_1; Y_2 | V_2, U) + \delta'. \] \tag{41}

Remark 5: In order to get the second bound on \(R_1\), we employ the requirement that not only receiver 1 can decode the message \(W_1\) successfully, but also receiver 2 can decode the message \(W_2\) successfully in (39) and (40) and, hence, we use Fano’s inequalities \((28a)\) and \((28b)\).

C. Outer Bound and Discussion

Combining the two upper bounds (37) with (41) and assuming that \(\delta\) and \(\delta'\) converge to 0, we have
\[ R_1 \leq \min \left[ I(V_1; Y_1 | U) - I(V_1; Y_2 | U), \right. \]
\[ I(V_1; Y_1 | V_2, U) - I(V_1; Y_2 | V_2, U) \left. \right]. \] \tag{42}

Similarly, we can bound \(R_2\) as
\[ R_2 \leq \min \left[ I(V_2; Y_2 | U) - I(V_2; Y_1 | U), \right. \]
\[ I(V_2; Y_2 | V_1, U) - I(V_2; Y_1 | V_1, U) \left. \right]. \] \tag{43}

Note that from (31) and (36) it follows that the joint distribution \( P(u, v_1, v_2, x_1, x_2, y_1, y_2) \) factors as (7) for the interference channel. For the broadcast channel, we replace \((X_1, X_2)\) by \(X \triangleq X_Q\). Now, the joint distribution \( P(u, v_1, v_2, x, y_1, y_2) \) factors as (11).

To consider the sum rate we let
\[ \Delta_1 = I(V_1; Y_1 | U) - I(V_1; Y_2 | U), \]
\[ \Delta_2 = I(V_2; Y_2 | U) - I(V_2; Y_1 | U), \]
\[ \Theta_1 = I(V_1; Y_1 | V_2, U) - I(V_1; Y_2 | V_2, U), \]
\[ \Theta_2 = I(V_2; Y_2 | V_1, U) - I(V_2; Y_1 | V_1, U). \]

The bounds (42) and (43) imply the following bounds on the sum rate:
\[ R_1 + R_2 \leq \Delta_1 + \Delta_2, \] \tag{44}
\[ R_1 + R_2 \leq \Theta_1 + \Theta_2, \] \tag{45}
\[ R_1 + R_2 \leq \min[\Delta_1 + \Theta_2, \Delta_2 + \Theta_1]. \] \tag{46}

Lemma 1: \(\min[\Delta_1 + \Theta_2, \Delta_2 + \Theta_1] \leq \Delta_1 + \Delta_2 = \Theta_1 + \Theta_2\).

Proof: We provide the proof in the Appendix.

It is interesting to further analyze the outer bound by comparing bounds (37) and (41). By assuming that \(\delta\) and \(\delta'\) converge to 0, the difference between these two bounds is
\[ R_{1, \Delta} \triangleq \Delta_1 - \Theta_1 = I(V_1; V_2 | Y_2, U) - I(V_1; V_2 | Y_1, U) = I(W_1; W_2 | Y_2, U) - I(W_1; W_2 | Y_1, U). \] \tag{47}

We observe that, in general, the difference between bounds (37) and (41) is non-zero.

V. INNER BOUND

A. Interference Channel with Confidential Messages

In this subsection we derive the achievable rate region for the interference channel. We prove that the region \(R_{IC}^{(31)}\) is achievable. The coding structure for the IC-CM is illustrated in Fig. 6. We employ an auxiliary random variable \(U\) in the sense of Han-Kobayashi [21] and two equivocation codebooks (stochastic encoders), one for each message \(W_1\) and \(W_2\). Encoder \(I\) maps \(v_i\) into a channel input \(x_i\). More precisely, the random code generation is as follows.

Fix \(P(u), P(v_1 | u)\) and \(P(v_2 | u)\), and
\[ P(x_1, x_2 | v_1, v_2) = P(x_1 | v_1)P(x_2 | v_2) \]
and let
\[ R_1' \triangleq I(V_1; V_2 | V_2, U) - \epsilon_1 \] \tag{48}
\[ R_2' \triangleq I(V_2; V_1 | V_1, U) - \epsilon_1 \] \tag{49}
where \(\epsilon_1 > 0\) and \(\epsilon_1\) is small for sufficiently large \(n\).
Fig. 6. Code construction for IC-CM

- [codebook generation] Randomly generate a typical sequence \( u \) with probability
  \[
P(u) = \prod_{i=1}^{n} P(u_i),
  \]
  and assume that both transmitters and receivers know the time-sharing sequence \( u \).

For transmitter \( t \), \( t = 1, 2 \), generate \( Q_t = 2^{n(R_t + R'_t)} \) independent sequences \( v_t \) each with probability
  \[
P(v_t | u) = \prod_{i=1}^{n} P(v_{t,i} | u_i)
  \]
  and labeled as
  \[
v_t(w_t, k_t), \; w_t \in \{1, \ldots, M_t\}, \; k_t \in \{1, \ldots, M'_t\}
  \]
where \( M_t = 2^{nR_t} \) and \( M'_t = 2^{nR'_t} \). Without loss of generality, \( M_t, M'_t \), and \( Q_t \) are assumed to be integers. Let
  \[
  C_t \triangleq \{ v_t(w_t, k_t) \}, \text{ for all } (w_t, k_t) \]
be the codebook of Transmitter \( t \). Its \( w_t \)-th sub-codebook (bin)
  \[
  C_t(w_t) \triangleq \{ v_t(w_t, k_t) \}, \text{ for } k_t = 1, \ldots, M'_t
  \]
follows the partitioning in (50).

- [encoding] To send a message pair
  \[
  (w_1, w_2) \in W_1 \times W_2,
  \]
each transmitter employs a stochastic encoder. Encoder \( t \) randomly chooses an element \( v_t(w_t, k_t) \) from the sub-codebook \( C_t(w_t) \). Transmitters generate the channel input sequences based on respective mappings \( P(x_t | v_t) \) and \( P(x_2 | v_2) \).

- [decoding] Given a typical sequence \( u \), let \( A^{(n)}(P_{V_t,Y_t | U}) \) denote the set of jointly typical sequences \( v_t \) and \( y_t \) with respect to \( P(v_t, y_t | u) \) [5]. Decoder \( t \) chooses \( w_t \) so that
  \[
  (v_t(w_t, k_t), y_t) \in A^{(n)}(P_{V_t,Y_t | U})
  \]
when such \( w_t \) exists and is unique; otherwise, an error is declared.

1) Error Probability Analysis: To bound the probability of error, we define the event
  \[
  E_e(w_1, k_1) \triangleq \{ (v_1(w_1, k_1), y_1) \in A^{(n)}(P_{V_1,Y_1 | U}) \}.
  \]
Without loss of generality, we can assume that transmitter 1 sends the message \( w_1 = 1 \) associated with the codeword \( v_1(1, 1) \), and define the corresponding event
  \[
  K_1 \triangleq \{ v_1(1, 1) \text{ sent} \}.
  \]
The union bound on the error probability of receiver 1 is as follows
  \[
P_{e,1} \leq P \left( \bigcap_{k_1} E_1^{e}(1, k_1) | K_1 \right) + \sum_{w_1 \neq 1, k_1} P\{ E_1(w_1, k_1) | K_1 \} 
  \]
  \[
  \leq P\{ E_1^{e}(1, 1) | K_1 \} + \sum_{w_1 \neq 1, k_1} P\{ E_1(w_1, k_1) | K_1 \}
  \]
where \( E_1^{e}(1, k_1) \) denotes the event
  \[
  \{(v_1(1, k_1), y_1) \notin A^{(n)}(P_{V_1,Y_1 | U})\}.
  \]
Following the joint asymptotic equipartition property (AEP) [5], we have
  \[
P\{ E_1^{e}(1, 1) | K_1 \} \leq \epsilon,
  \]
and, for \( w_1 \neq 1 \),
  \[
P\{ E_1(w_1, k_1) | K_1 \} \leq 2^{-n[1/(V_1; Y_1 | U) - \epsilon]}
  \]
Hence, we can bound the probability of error as
  \[
P_{e,1} \leq \epsilon + Q_1 2^{-n[1/(V_1; Y_1 | U) - \epsilon]}
  \]
  \[
  = \epsilon + 2^{n(R_t + R'_t)} 2^{-n[1/(V_1; Y_1 | U) - \epsilon]}
  \]
So, if
  \[
  R_t + R'_t < I(V_1; Y_1 | U),
  \]
then for any \( \epsilon_0 > 0 \), \( P_{e,1} \leq \epsilon_0 \) for sufficiently large \( n \). Similarly, for receiver 2, if
  \[
  R_2 + R'_2 < I(V_2; Y_2 | U),
  \]
then \( P_{e,2} \leq \epsilon_0 \) for sufficiently large \( n \). Hence, \( P_{e} \leq \epsilon_0 \) as long as the rate pair \( (R_1, R_2) \in \mathcal{R}_{IC}(\pi_{IC-1}) \).

2) Equivocation Calculation: To show that [54] holds, we consider the following equivocation lower bound
  \[
  H(W_1 | Y_2) \geq H(W_1 | Y_2, V_2, U)
  \]
where inequality [51] is due to the fact that conditioning reduces entropy. By applying the entropy chain rule [5], [51] can be expanded as follows
  \[
  H(W_1 | Y_2)
  \]
  \[
  \geq H(W_1, Y_2 | V_2, U) - H(Y_2 | V_2, U)
  \]
  \[
  = H(W_1, V_1, Y_2 | V_2, U)
  \]
  \[
  - H(V_1 | Y_2, V_2, U, W_1) - H(Y_2 | V_2, U)
  \]
  \[
  = H(W_1, V_1 | V_2, U) - H(V_1 | Y_2, V_2, U, W_1)
  \]
  \[
  - H(Y_2 | V_2, U) + H(Y_2 | V_1, V_2, U, W_1).
  \]
Based on functional dependence graphs [27] and the random code construction, we can show that the following is a Markov chain
  \[
  W_1 \rightarrow (V_1, V_2, U) \rightarrow Y_2
  \]
which yields
  \[
  I(W_1; Y_2 | V_1, V_2, U) = 0.
  \]
Hence, by using (52) and (53), we obtain
\[
H(W_1|Y_2) \geq H(W_1, V_1|V_2, U) - H(V_1|Y_2, V_2, U, W_1)
- H(Y_2|V_2, U) + H(Y_2|V_1, V_2, U)
= H(W_1, V_1|V_2, U) - H(V_1|Y_2, V_2, U, W_1)
- I(V_1:Y_2|V_2, U)
\geq H(V_1|V_2, U) - H(V_1|Y_2, V_2, U, W_1)
- I(V_1:Y_2|V_2, U).
\]

(54)

We consider the first term in (54). Note that given U = u, V_1 and V_2 are independent and V_1 has Q_1 possible values with equal probability. Hence,
\[
H(V_1|U, V_2) = H(V_1|U)
= \log Q_1
= n(R_1 + R_1').
\]

(55)

We next show that \( H(V_1|Y_2, V_2, U, W_1) \leq ne_2 \), where \( e_2 \) is small for sufficiently large \( n \). In order to calculate the conditional entropy \( H(V_1|Y_2, V_2, U, W_1) \), we consider the following situation. We fix \( W_1 = w_1 \), and assume that transmitter 1 transmits a codeword \( v_1(w_1, k_1) \in C_1(w_1) \), for \( 1 \leq k_1 \leq M_1 \), and that receiver 2 knows the sequences \( V_2 = v_2 \) and \( U = u \). Given index \( W_1 = w_1 \), receiver 2 decodes the codeword \( v_1(w_1, k_1) \) based on the received sequence \( y_2 \). Let \( \lambda(w_1) \) denote the average probability of error of decoding the index \( k_1 \) at receiver 2. Based on joint typicality [5, Chapter 8], we have the following lemma.

**Lemma 2:** \( \lambda(w_1) \leq \epsilon_0 \) for sufficiently large \( n \).

**Proof:** We provide the proof in the Appendix.

Fano’s inequality implies that
\[
\frac{1}{n} H(V_1|Y_2, V_2, U, W_1 = w_1) \leq \frac{1}{n} [1 + \lambda(w_1) \log M_1']
\leq \frac{1}{n} + \epsilon_0 I(V_1; Y_2|U)
\leq \epsilon_2.
\]

(56)

where the second inequality follows from Lemma 2 and (48).

Consequently,
\[
\frac{1}{n} H(V_1|Y_2, V_2, U, W_1)
= \frac{1}{n} \sum_{w_1 \in W_1} P(W_1 = w_1) H(V_1|Y_2, V_2, U, W_1 = w_1)
\leq \epsilon_2.
\]

(57)

Finally, the third term in (54) can be bounded based on the following lemma.

**Lemma 3:**
\[
I(V_1; Y_2|V_2, U) \leq n I(V_1; Y_2|V_2, U) + n\epsilon_3
\]

(58)

where \( \epsilon_3 \) is small for sufficiently large \( n \).

**Proof:** We provide the proof in the Appendix.

By using (53), (57), and (58), we can rewrite (54) as
\[
\frac{1}{n} H(W_1|Y_2) \geq R_1 + R_1' - I(V_1; Y_2|V_2, U) - \epsilon_2 - \epsilon_3.
\]

By the definition of \( R_1 \) (48), we have
\[
R_1 - \frac{1}{n} H(W_1|Y_2, X_2, W_2) \leq \epsilon_4
\]

(59)

where \( \epsilon_4 \triangleq \epsilon_1 + \epsilon_2 + \epsilon_3 \), and, thus, the security condition (52) is satisfied. Following the same approach, we can prove that (50) is satisfied.

**B. Broadcast Channel with Confidential Messages**

We next prove Theorem 4 based on the double-binning scheme which combines the Gel’fand-Pinsker binning [23] and the random binning. In this subsection we redefine the parameters \( R_1, R_2, R_1', R_2', Q_1, Q_2, M_1, \) and \( M_2 \). The coding structure for the BC-CM is shown in Fig. 7. We employ a joint encoder to generate two equivocation codewords \( v_1 \) and \( v_2 \), one for each message \( W_1 \) and \( W_2 \). The equivocation codewords are mapped into the channel input \( x \). The details of random code generation are as follows.

We fix \( P(u) \), \( P(v_1|u) \) and \( P(v_2|u) \), as well as \( P(x|v_1, v_2) \). Let \( 0 \leq \alpha \leq 1 \),
\[
R_1' \triangleq I(V_1; Y_2; V_2, U) - \epsilon_1'
\]
\[
R_2' \triangleq I(V_2; Y_1; V_1, U) - \epsilon_1'
\]

(60)

and
\[
R_t' \triangleq I(V_t; V_2|U) + \epsilon_t'
\]

(61)

where \( \epsilon_1' > 0 \) and \( \epsilon_t' \) is small for sufficiently large \( n \).

- [codebook generation] We generate randomly a typical sequence \( u \) with probability
\[
P(u) = \prod_{i=1}^{n} P(u_i)
\]

and assume that both the transmitter and the receivers know the sequence \( u \).

We generate \( Q_t = 2^{n(R_t + R_t' + R_t')} \) independent sequences \( v_t \) each with probability
\[
P(v_t|u) = \prod_{i=1}^{n} P(v_{t,i}|u_i)
\]

and label them
\[
v_t(w_t, s_t, k_t), \quad w_t \in \{1, \ldots, M_t\}, \quad s_t \in \{1, \ldots, J_t\}, \quad k_t \in \{1, \ldots, G_t\}.
\]

(62)

where \( M_t = 2^{nR_t}, \quad J_t = 2^{nR_t'}, \quad \) and \( G_t = 2^{nR_t'} \). Without loss of generality \( Q_t, M_t, J_t, \) and \( G_t \) are considered to be integers. Let
\[
C_t \triangleq \{v_t(w_t, s_t, k_t), \text{ for all } (w_t, s_t, k_t)\}
\]
encoder can not find an appropriate jointly typical pair, i.e., that

\[ \text{DISCRETE MEMORYLESS INTERFERENCE AND BROADCAST CHANNELS WITH CONFIDENTIAL MESSAGES: SECRECY RATE REGIONS} \]

1) Error Probability Analysis:

For a given typical sequence

\[ [\text{decoding}] \]

To send the message pair \( u \) where \( u = v_1(1,1), v_2(1,2) \), the encoder employs a stochastic encoder. We randomly choose a sub-bin \( C_t(w_t, s_t) \) from the bin \( C_t(w_t) \), for \( t = 1, 2 \). Next, we select a pair \( (k_1, k_2) \) so that

\[
(v_1(w_1, s_1, k_1), v_2(w_2, s_2, k_2)) \in A^{(n)}_{e}(P_{v_1,v_2}|U),
\]

where \( A^{(n)}_{e}(P_{v_1,v_2}|U) \) denotes, for a given typical sequence \( u \), the set of jointly typical sequences \( v_1 \) and \( v_2 \) with respect to \( P(v_1, v_2|U) \). If there are more than one such pairs, then we randomly select one. We generate the channel input sequence \( x \) according to the mapping \( P(x|v_1, v_2) \).

- [encoding] For a given typical sequence \( u \), let \( A_{e}^{(n)}(P_{v_1,y_1}|U) \) denote the set of jointly typical sequences \( v_1 \) and \( y_1 \) with respect to \( P(v_1, y_1|U) \). Decoder \( t \) chooses \( w_t \) so that \( (v_t(w_t, s_t, k_t), y_t) \in A_{e}^{(n)}(P_{v_t,y_t}|U) \) if such \( w_t \) exists and is unique; otherwise, an error is declared.

1) Error Probability Analysis: Without loss of generality, we assume that the message pair is \( (w_1 = 1, w_2 = 1) \) and that \( s_1 = s_2 = 1 \). First, we consider the error event \( T \) that the encoder can not find an appropriate jointly typical pair, i.e.,

\[
T = \{(v_1(1,1,k_1), v_2(1,1,k_2)) \notin A^{(n)}_{e}(P_{v_1,v_2}|U),
\text{ for } s_t = 1, \ldots, s_t, \ k_t = 1, \ldots, G_t, \text{ and } t = 1, 2 \}.
\]

The definition of \( R^t \) in (61) implies that

\[
R^t > I(V_1; V_2|U).
\]  

(63)

Hence, following the approach of [28], we have that

\[
P\{T\} \leq \delta_3
\]

(64)

where \( \delta_3 > 0 \) and \( \delta_3 \) is small for sufficiently large \( n \). In other words, the encoding is successful with probability close to 1 as long as \( n \) is large.

In the following, we assume that \( (v_1(1,1,1), v_2(1,1,1)) \) is sent and define the event

\[
K_2 \triangleq \{(v_1(1,1,1), v_2(1,1,1)) \in A^{(n)}_{e}(P_{v_1,v_2}|U)\}.
\]

Now, the error probability at receiver 1 is bounded as follows

\[
P_{e,1} \leq P\{T\} + (1 - P\{T\}) \left[ P\left( \bigcap_{s_1,k_1} E_1^{(n)}(s_1, k_1) | K_2 \right) \right]
\]

\[
+ \sum_{w_1 \neq 1} \sum_{s_1,k_1} P\{E_1(w_1, s_1, k_1) | K_2 \}
\]

\[
\leq P\{T\} + P\{E_1^{(n)}(1,1,1) | K_2 \}
\]

\[
+ \sum_{w_1 \neq 1} \sum_{s_1,k_1} P\{E_1(w_1, s_1, k_1) | K_2 \}
\]

where

\[
E_1(w_1, s_1, k_1) = \{(v_1(w_1, s_1, k_1), y_1) \in A^{(n)}_{e}(P_{v_1,y_1}|U)\}.
\]

Joint typicality [5, Chapter 14] implies that

\[
P\{E_1^{(n)}(1,1,1) | K_2 \} \leq \epsilon,
\]

\[
P\{E_1(w_1, s_1, k_1) | K_2 \} \leq 2^{-n[I(V_1; Y_1|U) - \epsilon]} \text{ for } w_1 \neq 1.
\]

Hence, we can bound the probability of error as

\[
P_{e,1} \leq \delta_3 + \epsilon + Q_1 2^{-n[I(V_1; Y_1|U) - \epsilon]}
\]

(65)

So, if

\[
R_1 + R_2 + R^t < I(V_1; Y_1|U),
\]

(66)

then for any \( \epsilon_0 > 0 \), \( P_{e,1} \leq \epsilon_0 \) for sufficiently large \( n \). Similarly, for receiver 2, if

\[
R_2 + R^t + R^t < I(V_2; Y_2|U),
\]

(67)

then \( P_{e,2} \leq \epsilon_0 \) for sufficiently large \( n \). Hence, (2), (60), (61), (65), and (67) imply that \( P_{e} \leq \epsilon_0 \) as long as the rate pair \( (R_1, R_2) \) is \( \pi_{BC}(\pi_{BC}) \).

2) Equivocation Calculation: We next prove that the secrecy requirement (53) holds for BC-CM. Following the same approach as (51), we have

\[
H(W_1|Y_2) \geq H(V_1|V_2, U) - H(V_1|Y_2, V_2, U, W_1) - I(V_1; Y_2|V_2, U).
\]

(68)

Consider the first term in (68)

\[
H(V_1|U, V_2) = H(V_1|U) - I(V_1; V_2|U).
\]

Note that given \( U = u \), \( V_1 \) attains \( Q_1 \) possible values with equal probability. Hence, we have \( H(V_1|U) = \log Q_1 \). Using the same approach as in Lemma 3, we can obtain

\[
I(V_1; V_2|U) \leq nI(V_1; V_2|U) + n\epsilon_2,
\]

(69)
Similarly, Gaussian wiretap channels have recently been proposed in \cite{29}. A challenging problem is code constructions for a binary-input interference channels under information-theoretic secrecy. In and compared several transmission schemes for Gaussian channel. We presented a special case of IC-CM for which the messages. The obtained results offer insights into the two (5a) is satisfied. Following the same approach, we can prove \[ H(V_1|Y_2, V_2, U, W_1) \leq n\epsilon'_3 \] where \( \epsilon'_3 \) is small for sufficiently large \( n \). Applying Lemma \[ \text{and } 68 \] the third term in \( 68 \) can be bounded as \[ I(V_1; Y_2|V_2, U) \leq n I(V_1; V_2|V_2, U) + n\epsilon'_4 \] \[ = n(R_1' + \epsilon'_1 + \epsilon'_4) \] (71) where \( \epsilon'_4 \) is small for sufficiently large \( n \) and the equality \( 71 \) follows from the definition \( 60 \). Hence, by using \( 69 \), \( 70 \), and \( 71 \), we can rewrite \( 68 \) as \[ \frac{1}{n} H(V_1|Y_2) \geq R_1 - \epsilon'_5 \] where \( \epsilon'_5 \triangleq \epsilon'_1 + \epsilon'_2 + \epsilon'_3 + \epsilon'_4 \), and thus the security condition \( 58 \) is satisfied. Following the same approach, we can prove that \( 56 \) also holds.

VI. CONCLUSION

We derived the outer and the inner bounds on the capacity of the interference and broadcast channels with confidential messages. The obtained results offer insights into the two communication problems. The difference in the outer bound reflects the fact that the joint encoding at the transmitter can only be performed in the BC-CM whereas in the IC-CM, encoders offer different channel inputs. The achievability proof suggests the code construction appropriate for these channel. We presented a special case of IC-CM for which the two bounds meet to describe the capacity region. We proposed and compared several transmission schemes for Gaussian interference channels under information-theoretic secrecy. In particular, the encoding scheme in which transmitters dedicate some of their power to create artificial noise was shown to outperform both time-sharing and simultaneous transmission of messages sent with the optimal power. However, constructing practical wiretap codes that can achieve the derived rates is a challenging problem. Code constructions for a binary-input Gaussian wiretap channel have recently been proposed in \cite{29}.

APPENDIX

Proof: (Lemma 1) By the definition of \( \Delta_1 \), we have \[ \Delta_1 = I(V_1; Y_1|U) - I(V_1; V_2|U) \] \[ = I(V_1; V_2; Y_1|U) - I(V_2; Y_2|V_1, U) \] \[ - I(V_1, V_2; Y_2|U) + I(V_2; Y_2|V_1, U). \] (72)

Similarly, \[ \Delta_2 = I(V_2; Y_2|U) - I(V_2; Y_1|U) \] \[ = I(V_1, V_2; Y_2|U) - I(V_1; Y_2|V_2, U) \] \[ - I(V_1, V_2; Y_2|U) + I(V_1; Y_1|V_2, U). \] (73)

and \( 72 \) imply that \[ \Delta_1 + \Delta_2 = -I(V_2; Y_2|V_2, U) + I(V_1; Y_1|V_1, U) - I(V_2; Y_1|V_1, U) + I(V_1, V_2; Y_2|U) - I(V_1; Y_2|V_2, U) \] \[ = \Theta_2 + \Theta_1. \] (74)

Note that \[ 2(\Delta_1 + \Delta_2) = 2(\Theta_1 + \Theta_2) \] \[ = (\Delta_1 + \Theta_2) + (\Delta_2 + \Theta_1) \]

Hence, \[ \min[\Delta_1 + \Theta_2, \Delta_2 + \Theta_1] \leq \Delta_1 + \Delta_2 = \Theta_1 + \Theta_2. \]

We have the derived results.

Proof: (Lemma 2) For a given typical sequence pair \((v_2, u)\), let \( A^{(n)}(P_{V_1, V_2|V_2, U}) \) denote the set of jointly typical sequences \( v_1 \) and \( y_2 \) with respect to \( P(v_1, y_2|v_2, u) \). For a given \( W_1 = w_1 \), decoder 2 chooses \( k_2 \) so that \[ (v_1(w_1, k_1), y_2) \in A^{(n)}(P_{V_1, V_2|V_2, U}) \] if such \( k_1 \) exists and is unique; otherwise, an error is declared. Define the event \[ E(k_1) = \{(v_1(w_1, k_1), y_2) \in A^{(n)}(P_{V_1, V_2|V_2, U})\}. \]

Without loss of generality, we assume that \( v_1(w_1, k_1) = 1 \) was sent, and define the event \[ \hat{K}_1 = \{v_1(w_1, 1) \text{ sent}\}. \]

Hence \[ \lambda(w_1) \leq P\{E^c(k_1) = 1|\hat{K}_1\} + \sum_{k_1 \neq 1} P\{E(k_1)|\hat{K}_1\} \] where \( E^c(k_1) = 1 \) denotes the event \[ \{(v_1(w_1, 1), y_2) \notin A^{(n)}(P_{V_1, V_2|V_2, U})\}. \]

Following the joint AEP \cite{5}, we have \[ P\{E^c(k_1) = 1|\hat{K}_1\} \leq \epsilon, \] and, for \( k_1 \neq 1, \]

\[ P\{E(k_1)|\hat{K}_1\} \leq 2^{-n[I(V_1; V_2|V_2, U) - \epsilon]}. \]

Now, we can bound the probability of error as \[ \lambda(w_1) \leq \epsilon + M_1 2^{-n[I(V_1; V_2|V_2, U) - \epsilon]} \leq \epsilon + 2^{n R'_1 - 2^{-n[I(V_1; Y_2|V_2, U) - \epsilon]}}. \]

Note that \( R'_1 = I(V_1; Y_2|V_2, U) - \epsilon_1 \). Hence, by choosing \( \epsilon_1 > \epsilon \), we have \[ \lambda(w_1) \leq \epsilon_0 \] where \( \epsilon_0 \) is small for sufficiently large \( n \).

Proof: (Lemma 3) Let \( A^{(n)}(P_{U, V_1, V_2, Y_2}) \) denote the set of typical sequences \( (u, v_1, v_2, y_2) \) with respect to \( P(u, v_1, v_2, y_2) \), and \[ \mu(u, v_1, v_2, y_2) = \begin{cases} 1, & (u, v_1, v_2, y_2) \notin A^{(n)}(P_{U, V_1, V_2, Y_2}) \\ 0, & \text{otherwise} \end{cases} \]
be the corresponding indicator function.

We expand \( I(V_1; Y_2 | V_2, U) \) as

\[
I(V_1; Y_2 | V_2, U) \leq I(V_1; Y_2 | V_2, U) + I(\mu; Y_2 | V_2, U)
\]

\[
= \sum_{j=0}^{1} P(\mu = j) I(V_1; Y_2 | V_2, U, \mu = j) + I(\mu; Y_2 | V_2, U)
\]  

(75)

Note that

\[
P(\mu = 1) I(V_1; Y_2 | V_2, U, \mu = 1) \leq n P[u, v_1, v_2, y_2 \notin A^{(n)}_1(P(U, V_1, V_2, Y_2))] \log |Y_2|
\]

\[
\leq n e \log |Y_2|,
\]  

(76)

and

\[
I(\mu; Y_2 | V_2, U) \leq H(\mu) \leq 1.
\]  

(77)

We only consider the term \( P(\mu = 0) I(V_1; Y_2 | V_2, U, \mu = 0) \).

Following the sequence joint typicality properties \([5]\), we have

\[
P(\mu = 0) I(V_1; Y_2 | V_2, U, \mu = 0) \leq I(V_1; Y_2 | V_2, U, \mu = 0)
\]

\[
= \sum_{(u, v_1, v_2, y_2) \in A^{(n)}} P(u, v_1, v_2, y_2) [\log P(\nu_i, v_1, v_2) - \log P(y_2 | v_2, u) - \log P(v_1 | v_2, u)]
\]

\[
\leq n[H(Y_2 | V_2, U) + H(V_1 | V_2, U) - H(V_1, Y_2 | V_2, U) + 3\epsilon]
\]

\[
= n I(V_1; Y_2 | V_2, U) + 3\epsilon.
\]  

(78)

Combining (75), (76), (77), and (78), we have the desired result

\[
I(V_1; Y_2 | V_2, U) \leq n I(V_1; Y_2 | V_2, U)
\]

\[
+ n \left( \epsilon \log |Y_2| + 3\epsilon + \frac{1}{n} \right)
\]

\[
= n I(V_1; Y_2 | V_2, U) + n\epsilon_3
\]

where

\[
\epsilon_3 \triangleq \epsilon \log |Y_2| + 3\epsilon + \frac{1}{n}.
\]

Proof: (Theorem 5) Since the switch channel is a special case of the interference channel, we focus on the outer bound \([9]\) and the inner bound \([10]\) and prove that

\[
\mathbb{R}_O(\pi_{IC-O}) = \mathbb{R}_I(\pi_{IC-I})
\]

for the SC-CM case.

We note that the distribution \(\pi_{IC-I}\) implies that, for a given \(U\), auxiliary random variables \(V_1\) and \(V_2\) are independent, but this may not hold for the distribution \(\pi_{IC-O}\). Hence, we need to first show that the condition

\[
I(V_1; V_2 | U) = 0
\]  

(79)

holds in the outer bound for SC-CM. Furthermore, if

\[
I(V_1; V_2 | Y_2, U) = 0
\]  

(80)

also holds in the outer bound for SC-CM, then we have

\[
I(V_1; Y_2 | V_2, U) = I(V_1; Y_2 | U) + I(V_1; V_2 | Y_2, U)
\]

\[
- I(V_1; V_2 | U)
\]

\[
= I(V_1; Y_2 | U),
\]

\[
I(V_2; Y_2 | V_1, U) = I(V_2; Y_2 | U) + I(V_1; V_2 | Y_2, U)
\]

\[
- I(V_1; V_2 | U)
\]

\[
= I(V_2; Y_2 | U),
\]  

(81)

that is, the outer bound \([9]\) meets the inner bound \([10]\).

Now, we prove that conditions (79) and (80) hold in the outer bound for SC-CM. By definitions (31) and (36), we need to show that

\[
I(W_1; W_2 | U_i) = 0
\]  

(82)

\[
I(W_1; W_2 | U_i, Y_2) = 0
\]  

(83)

where \(U_i = \{Y_1^{i-1}, Y_2^{i+1}\}\). We first prove the equality (82).

Following the switch output definition \([19]\), we have

\[
\{Y_1^{i-1}, Y_2^{i+1}\} = \{Z_1^{i-1}, Z_2^{i+1}, S_1^{i-1}, S_2^{i+1}\}
\]  

(84)

and hence,

\[
I(W_1; W_2 | U_i)
\]

\[
= I(W_1; W_2 | Z_1^{i-1}, Z_2^{i+1}, S_1^{i-1}, S_2^{i+1})
\]

\[
= \sum_{s_1^{i-1}, s_2^{i+1}} P(S_1^{i-1} = s_1^{i-1}, Z_2^{i+1} = s_2^{i+1}) I(W_1; W_2 | Z_1^{i-1}, Z_2^{i+1}, S_1^{i-1}, S_2^{i+1})
\]

\[
= \sum_{s_1^{i-1}, s_2^{i+1}} \prod_{j=1}^{i} P(S_1^{j-1} = s_1^{j-1}) \prod_{k=1}^{j+1} P(S_2^{k} = s_2^{k})
\]

(85)

\[
= I(W_1; W_2 | Z_1^{i-1}, Z_2^{i+1}, S_1^{i-1}, S_2^{i+1}).
\]  

(86)

Now, for a given \(S_{i,j}\), the switch channel model \([18]\) implies that \(Z_{i,j}\) only depend on the channel input \(X_{s_{i,j}}\). By using functional dependence graphs \([27]\), we can easily verify that

\[
I(W_1; W_2 | Z_1^{i-1}, Z_2^{i+1}, S_1^{i-1}, S_2^{i+1}) = 0
\]

for fixed switch state information \(S_1^{i-1}, S_2^{i+1}\). Hence, (86) implies that \(I(W_1; W_2 | U_i) = 0\). Following the same approach, we can prove the equality (83). Therefore, we have the desired result.

\[\square\]

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