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Experimental corroboration of the thermoelectric performance of Bi$_2$PdO$_4$ oxide and Pb-doped derivatives

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Abstract

A theoretical study has recently revealed Bi$_2$PdO$_4$ as a promising p-type oxide thermoelectric material, with excellent electrical properties and low thermal conductivity, due to its structural peculiarities. Polycrystalline samples of the pristine material and Pb-doped Bi$_{1.9}$Pb$_{0.1}$PdO$_4$ have been prepared by a conventional solid-state reaction, and an exhaustive structural characterization has been performed by high-energy synchrotron x-ray diffraction. Thermoelectric transport properties have been measured in the 300 – 800 K temperature range. The undoped compound displays p-type semiconductor behaviour and extremely high values of thermopower, up to 1458 $\mu$V K$^{-1}$ at 340 K, along with low lattice thermal conductivity, related to large vibrations of Bi and O atoms. In the Pb-doped derivative the electrical resistivity is greatly enhanced, which along with a reduction of the lattice thermal conductivity results in an improved thermoelectric performance by more than one order of magnitude. These features underline the promising further optimization of this material aiming at thermoelectric applications.

Introduction

Thermoelectric materials have attracted vast attention for many decades due to their capacity to interconvert heat and electricity.\cite{1,2} These materials provide a unique opportunity to recover waste heat energy and transform it directly into electricity, or to produce a temperature gradient when electricity is supplied. Therefore, they are ideal candidates for applications such as power generators, thermal energy sensors, coolers, etc.\cite{3} The performance of thermoelectric devices is measured by using the figure of merit $ZT$, which determines the theoretical fraction of the Carnot efficiency that can be reached by a thermoelectric material. It is defined as $ZT = (S^2\sigma T)/(\kappa_L + \kappa_e)$, where $S$ is the Seebeck coefficient, $\sigma$ is the electrical conductivity, $\kappa_L$ is the lattice thermal conductivity, $\kappa_e$ is the electronic thermal conductivity and $T$ is the absolute temperature. We thus look for materials with large power factors ($S^2\sigma$), and low thermal conductivity. This is a challenge since the Seebeck coefficient and the electric conductivity change in opposite directions,
following the Pisarenko relation\(^4\). In addition to these parameters associated with the efficiency, thermoelectric materials require: i) to exhibit good chemical and mechanical stability, non-toxicity, ii) to show resistance to redox reactions and iii) to operate in a wide range of temperatures in air, to be competitive as commercial materials.

Since transition metal oxides fulfil these requirements, they offer a rich playground for developing promising thermoelectric materials and hence, in the last years the interest in this family of compounds has rapidly increased. The finding of great thermo-power value (characterised by the Seebeck coefficient) in the layered Na\(_x\)CoO\(_2\) oxides\(^5,6\) encouraged the scientific community to explore new transition metal oxides as potential thermoelectric materials, such as SrTiO\(_3\), a well-known n-type oxide with large power factor and other layered cobaltite compounds as La\(_{0.8}\)Sr\(_{0.2}\)CoO\(_3\), Ca\(_2\)Co\(_4\)O\(_9\) and Bi\(_2\)Sr\(_2\)CoO\(_4\), which display promising thermoelectric properties\(^9,10\). As enumerated herein, there are many advantages in using transition-metal oxides compared to other thermoelectric materials; for instance, the electronic properties can be easily tailored, they exhibit a broad range of electric properties as well as thermal behaviours, and the physics of the phonons in these compounds have been deeply studied and comprehended\(^11\). However, transition-metal oxides also present some drawbacks such as poor electrical conductivity with low charge-carrier mobility and high thermal conductivity. These values are contrary to the desired ones and yield low values of ZT. The most common chemical strategies to invert these values are chemically doping or modifying the stoichiometry, in order to create certain degree of crystal disorder, and introducing extra sites, which may contribute to hamper the phonon transport\(^12,13\). Recently, it has been demonstrated that s\(^2\) lone electron pairs of the p-block elements provoke anharmonic bonds in high-symmetry crystalline solids\(^14,15\). Last year, Jiangang He et al.\(^16\) suggested an alternative approach to develop new thermoelectric materials with a “lone pair cation” and a d\(^8\) cation in square-planar coordination, demonstrated via ab-initio calculations for Bi\(_2\)PdO\(_4\) oxide. On the one side, the use of oxides with a highly distorted oxygen environment originated from the lone pairs of Bi\(^{3+}\) cations is proposed to reduce the lattice thermal conductivity. On the other side, in order to increase the power factor, the localised Pd\(^{2+}\) d\(_z^2\) orbitals in a square planar arrangement contribute to stabilise a flat and disperse valence band structure. Therefore, Bi\(_2\)PdO\(_4\) was proposed to be an ideal candidate for thermoelectric applications.

In the present contribution, we have realized this theoretical approach by synthesizing and characterizing the thermoelectric properties of Bi\(_2\)PdO\(_4\), thus confirming that it fulfils the expectations. We present an exhaustive crystallographic analysis by means of high-energy x-ray synchrotron diffraction at different temperatures and the subsequent correlation with the thermoelectric properties. In fact, it presents Seebeck coefficients as high as 1218 \(\mu\)V K\(^{-1}\) at 750 K and a reduced (compared to other oxides) thermal conductivity of 1.5 W m\(^{-1}\) K\(^{-1}\) at this temperature. The interpretation of the experimental data, supported by the theoretical
calculation previously reported, has been essential to deeply understand the advantages and drawbacks of this oxide. This study represents the starting point to design new materials with enhanced properties, such as Bi_{2-x}Pb_{x}PdO_{4} where the charge-carriers density could be optimized\textsuperscript{17, 18}. Herein, the composition Bi\textsubscript{1.9}Pb\textsubscript{0.1}PdO\textsubscript{4} has also been investigated.

**Experimental**

Bi\textsubscript{2}PdO\textsubscript{4} and Bi\textsubscript{1.90}Pb\textsubscript{0.1}PdO\textsubscript{4} samples were prepared using conventional solid-state reaction. Stoichiometric amounts of Bi\textsubscript{2}O\textsubscript{3}, PdO and PbO were ground as acetone slurry and heated at 730 °C during 12h (2 min/degree rate). Then the samples were pressed into 12 mm pellets and sintered under the same experimental conditions (730 °C during 12h)\textsuperscript{19}.

The specimens, obtained as a brown well-crystallised powders, were initially characterised by laboratory x-ray diffraction, using a Bruker-AXS D8 diffractometer (40 kV, 30 mA), controlled by DRIFFACTPLUS software, in Bragg-Brentano reflection geometry with Cu K\textalpha radiation (\(\lambda = 1.5418 \text{ Å}\)) and a lynxeye detector. Further crystallographic analyses were carried out at the BL04-MSPD beamline of ALBA synchrotron in order to accurately identify and refine the crystal structure. Synchrotron x-ray diffraction (SXRD) patterns were collected in high angular resolution mode (so-called MAD set-up, Multicrystal Analyser Detectors), selecting an incident beam with 38 keV radiation (\(\lambda = 0.3511 \text{ Å}\)) \textsuperscript{20}. The samples were contained in 0.7 mm diameter quartz capillaries. Using high-energy synchrotron x-rays allowed collecting data on such absorbing material in transmission mode. SXRD data were recorded at 295 (RT), 573, 673 and 773 K to study potential phase transitions that may affect the thermoelectric properties. The Rietveld refinement\textsuperscript{21} of the crystal structure was performed using the FullProf suite \textsuperscript{22}. A pseudo-Voigt function was chosen to generate the line shape of the diffraction peaks. The scale factor, background coefficients, zero-point error, pseudo-Voigt corrected for asymmetry parameters, positional coordinates and isotropic thermal factors of the Bi (Pb), Pd and O atoms were refined in the final runs.

**Results and discussion**
As observed in Figure 1, the SXRD patterns show sharp and well-defined reflections, indexed in the $P4/ncc$ (# 130) tetragonal cell. In this model, Bi(Pb) atoms occupy the $8f$ ($x,-x$, $1/4$) Wyckoff positions, Pd atoms the $4c$ ($1/4$, $1/4$, $z$) sites and the oxygen anions are placed at the $16g$ $(x,y,z)$ sites. The Rietveld analysis resulted in a satisfactory agreement between the observed and calculated profiles. The occupancy factor for oxygen atoms confirmed a full stoichiometry. No impurities were detected in any case. For the Pb-doped sample, some reflection profiles are asymmetric and show a Lorentzian tail on the left side at low angles and on the right side at high angles (Fig. 1b); therefore, an instrumental parameters issue has been discarded. For this sample, the asymmetric broadening on all the patterns has been modelled using a distribution of the unit-cell parameters within the same space group. The introduction of a second phase with the following cell parameters $a_1=a_2$ and $c_1\neq c_2$, has led to a successful structural refinement as observed in the inset of Figure 1b. The asymmetry origin of the peaks could be ascribed to local inhomogeneous distribution of Pb, leading to Pb-rich areas. Unfortunately, it is not possible to refine the Bi and Pb occupancy by means of x-rays due to their similar scattering strength. A summary of selected internal parameters is displayed in Table 1 and Table 2. Some of the refined parameters for the doped sample is included in the Supplementary Information (Table S1).

![Figure 1](image-url)  
**Figure 1.** Observed (crosses), calculated (solid line) and difference (bottom) S-XRD Rietveld profiles for (a) Bi$_2$PdO$_4$ and (b) Bi$_{1.90}$Pb$_{0.1}$PdO$_4$ at 298 K collected at MSPD diffractometer (ALBA). The vertical green markers represent the positions of the space-group-allowed Bragg reflections. The remaining patterns at 573, 673 and 773 K are included in the Supplementary Information (Table S1).
The local environment and the internal parameters at room temperature and at high temperatures have been analysed. As it was predicted, the lone electron pairs $6s^2$ of Bi$^{3+}$ cause a large distortion in the [BiO$_6$] octahedra giving rise to three different bond distances: 2.32(1), 2.82(1) and 2.15(1) Å. These values are very close to the corresponding Bi-O distances described for Bi$_2$PdO$_4$ in Ref 15 (2.387, 2.716, 2.143 Å) or for the analogous cuprate Bi$_2$CuO$_4$ (2.3336(7) 2.7590(6) and 2.1280(6) Å).\textsuperscript{23, 24} The lack of a regular octahedral framework, which favours the anharmonicity, in combination with the lone pairs acting as a stereochemical barrier, both contribute to lower the lattice thermal conduction. The Pd$^{2+}$ cation is equidistant to four oxygen anions in a square-planar coordination forming one-dimensional Pd$^{2+}$ chains along $c$ without any connecting oxygen between them. Since the Pd-Pd interatomic distance is 2.995(3) Å at RT, the formation of direct Pd-Pd bonds is not excluded, and this fact has relevant implications in the electronic structure, as previously reported. Some schematic views of the structure are represented in Figure 2.
**Figure 2.** Schematic view of the crystal structure along the (a) [001] direction, (b) [100]/[010] direction, (c) representation of the unit cell and (d) the coordination polyhedra for Bi (yellow) and Pd (blue).

The thermal evolution of the SXRD diagrams show that the crystal structure of Bi$_2$PdO$_4$ remains tetragonal in the temperature range 298-773 K. The overall size of the unit-cell increases with temperature, as denoted by the volume expansion represented in Figure 3. Since the $a$-axis exhibits a subtle negative thermal expansion (8.62292(4) Å at 298 K and 8.62142(2) Å at 773 K) evolving in the opposite direction to the volume, the enlargement effect is exclusively associated with the variation of the $c$-axis, which undergoes a change from 5.91023(3) Å at 298 K to 5.98181(2) Å at 773 K. This effect can be observed in the evolution of the different peaks (see inset of Figure 1). While the reflections hkl are shifted towards lower 2θ as long as the temperature increases, the corresponding h00 slightly moves to higher angles. This unexpected tendency is also observed in the behaviour of one of the Bi-O distances, which decreases from 2.82(1) Å to 2.794(8) Å when temperature increases. Pd-O bond distances remain virtually constant, while Pd-Pd bond length expands linearly with temperature, as expected considering the way in which the unit-cell expands.

The valences of the cations, calculated from structural data using the bond-valence Brown’s model, confirm the presence of trivalent Bi$^{3+}$ and divalent Pd$^{2+}$. The square-planar coordination environment for Pd$^{2+}$ ions leads into a specific splitting in the energy level of the 4d orbitals with the d$_{z^2}$ orbitals becoming the highest level of the valence band, which is crucial in order to accomplish a flat (in the ab plane) and disperse (along the c-axis) band. The formation of direct Pd-Pd bonds along the chains of PdO$_4$ squares determines the electron delocalization along $c$, and affects the transport and thermoelectric properties, as discussed below.

The introduction of 5% of Pb$^{2+}$, with larger ionic size than Bi$^{3+}$ ($r$(Bi$^{3+}$)= 1.03 Å vs $r$(Pb$^{2+}$)= 1.19 Å), gives rise to an anisotropic variation of the unit-cell parameters. While the $a$-axis undergoes an elongation, the $c$-axis is shortened with respect to undoped compound. Unexpectedly, the overall effect produces a slight contraction of the lattice, as can be seen in the volume values, since the hole doping effect upon replacing trivalent Bi by divalent Pd predominates over the steric factor. The most relevant structural modification in the Pb- compound is the reduction of the Pd-Pd distance. This metal-metal bond length is directly related with the bandwidth and the band order; the shorter distance directly affects the electron delocalization and creates a better mobility path for charge carriers, increasing the electrical conductivity.
Figure 3. Thermal evolution of the unit-cell parameters and volume. The inset drawing represent the unit-cell.

An interesting insight into the crystal structure results from the localization of the lone electron pairs belonging to Bi$^{3+}$ ions. This can be unveiled from Difference Fourier synthesis from high-quality x-ray diffraction data, as those collected in the present work. The difference between observed and calculated structure factors contain invaluable information about missed electron density located in interatomic regions of the unit cell. Figure 4 shows the positive electronic density maps corresponding to the lone electron pairs of Bi. The electron density lobes are found at distances from Bi approximately equivalent to those expected for typical Bi-O bond, in the 2.1-2.5 Å range, as described elsewhere. As mentioned in the introduction, it is believed that the lone electron pairs contribute to phonon scattering, which substantially decreases the thermal conductivity of Bi$_2$PdO$_4$ oxide, within the limits of the best thermoelectric oxides that find applications in the intermediate temperature range between 700-900 K.
Figure 4. Difference Fourier synthesis from high-quality synchrotron x-ray diffraction data, highlighting the lobes of the Bi lone electron pairs, directed to an empty region of the unit cell.
Table 1. Unit-cell, atomic positions, thermal parameters and reliability factors for Bi$_2$PdO$_4$ obtained from SXRD data at room temperature, 573, 673 and 773 K.

|          | 298 K       | 573 K       | 673 K       | 773 K       |
|----------|-------------|-------------|-------------|-------------|
| a (Å)    | 8.62292(4)  | 8.62232(3)  | 8.62196(3)  | 8.62142(2)  |
| c (Å)    | 5.91023(3)  | 5.95078(2)  | 5.96635(2)  | 5.98181(2)  |
| V (Å$^3$)| 439.453(4)  | 442.107(3)  | 443.528(2)  | 444.621(2)  |
| Bi $8f$($x$,-$x$, ¼) |          |             |             |             |
| x        | -0.07953(7) | -0.07917(6) | -0.07908(6) | -0.07880(6) |
| $B_{iso}$(Å$^2$) | 0.83(2)    | 1.41(2)     | 1.60(2)     | 1.85(2)     |
| Pd $4c$ (¼,¼,¼,z) |             |             |             |             |
| z        | 0.0816(4)   | 0.0815(3)   | 0.0816(3)   | 0.0819(3)   |
| $B_{iso}$ (Å$^2$) | 0.19(4)    | 0.54(4)     | 0.69(4)     | 0.82(4)     |
| O $16g$ (x,y,z) |             |             |             |             |
| x        | 0.359(1)    | 0.357(1)    | 0.3574(9)   | 0.3578(9)   |
| y        | 0.046(1)    | 0.044(1)    | 0.0432(9)   | 0.0421(9)   |
| z        | 0.584(2)    | 0.587(2)    | 0.589(1)    | 0.588(1)    |
| $B_{iso}$ (Å$^2$) | 0.9(2)     | 1.7(2)      | 1.7(2)      | 2.1(2)      |

Reliability factors

|          | 298 K       | 573 K       | 673 K       | 773 K       |
|----------|-------------|-------------|-------------|-------------|
| $R_{Bragg}$ (%) | 3.88        | 3.32        | 3.31        | 3.63        |
| $R_p$ (%)  | 10.6        | 8.66        | 8.01        | 7.90        |
| $R_{wp}$ (%) | 14.6        | 11.8        | 10.7        | 10.8        |
| $R_{exp}$ (%) | 7.53        | 7.62        | 7.62        | 8.34        |
| $\chi^2$  | 3.75        | 2.39        | 1.98        | 1.95        |
Table 2. Main bond distances and bond valence calculation for Bi$_2$PdO$_4$ and Bi$_{1.9}$Pb$_{0.1}$PdO$_4$ obtained from S-XRD data at room temperature, 573, 673 and 773 K.

|                  | Bi$_2$PdO$_4$     | 298 K  | 573 K  | 673 K  | 773 K  |
|------------------|-------------------|--------|--------|--------|--------|
| Bi-O (Å)         | 2.32(1) x2        | 2.337(9) x2 | 2.349(9) x2 | 2.341(9) x2 |
|                  | 2.15(1) x2        | 2.167(9) x2 | 2.160(8) x2 | 2.160(8) x2 |
|                  | 2.82(1) x2        | 2.793(9) x2 | 2.790(8) x2 | 2.794(8) x2 |
| Pd-O (Å)         | 1.990(9) x4       | 2.003(9) x4 | 2.010(8) x4 | 2.019(3) x4 |
| Pd-Pd (Å)        | 2.955(3)          | 2.975(3)  | 2.983(3)  | 2.991(3)  |
| BVC (Bi)         | 3.06(4)           | 2.98(3)   | 2.98(3)   | 3.00(3)   |
| BVC (Pd)         | 2.34(3)           | 2.26(3)   | 2.22(2)   | 2.16(2)   |

|                  | Bi$_{1.9}$Pb$_{0.1}$PdO$_4$ | 298 K  | 573 K  | 673 K  | 773 K  |
|------------------|-------------------------------|--------|--------|--------|--------|
| Bi(Pb)-O (Å)     | 2.790(14)x2                  | 2.792(12)x2 | 2.810(14)x2 | 2.841(15)x2 |
|                  | 2.331(17)x2                  | 2.324(12)x2 | 2.286(17)  | 2.224(17)x2 |
|                  | 2.176(15)x2                  | 2.175(12)x2 | 2.177(15)x2 | 2.198(16)x2 |
| Pd-O (Å)         | 1.986(14)x4                 | 2.008(12)x4 | 2.040(14)x4 | 2.060(15)x4 |
| Pd-Pd (Å)        | 2.936(5)                    | 2.954(4)  | 2.961(4)  | 2.969(5)  |
| BVC (Bi)         | 3.12(6)                     | 3.14(4)   | 3.24 (6)  | 3.35(7)   |
| BVC (Pb)         | 2.74(4)                     | 2.76(3)   | 2.82(4)   | 2.88(4)   |
| BVC (Pd)         | 2.49(4)                     | 2.35(4)   | 2.15 (4)  | 2.04 (4)  |
Transport Properties

The electrical resistivity was obtained by combining a current source (Keithley 6220) with a nanovoltmeter (Keithley 2182A) in the Van der Pauw configuration. The Seebeck coefficient was measured in bar shaped samples by comparison with a reference constantan wire by using a commercial instrument from MMR technologies. These both magnitudes were determined from 300 K to 720 K. The electrical resistivity (Figure 5a) shows an exponential decay throughout the whole measurement range, in agreement with an intrinsic semiconductor behaviour. It falls from a maximum value over $10^3 \, \Omega \, m$ at 300 K to a minimum value of $1.9 \, \Omega \, m$ at 750 K. Two exponential regions can be distinguished, which can be attributed to different charge carriers activation processes. The first one arises from intrinsic defects that overcome the potential barriers of grain boundaries at lower temperatures, whereas the second one comes from thermal excitation across the band gap at higher temperature. It is possible to evaluate the high-temperature behaviour (>500 K) using an exponential fit, for which the activation energy of charge carriers is determined as 0.42 eV. This value lies well within the energy range calculated by DFT for PBE functionals (0.15 eV), and that determined for HSE06 functionals (1.41 eV). The resistivity values are still much higher than those found in the theoretical study performed by J. He et al.\(^\text{16}\) of the order of $10^5 \, \Omega \, m$. This difference is probably associated with a low carrier concentration and the scattering mechanisms of charge carriers in the sample. Furthermore, our study is focused on polycrystalline samples, while theoretical calculations discuss an ideal single crystal, and grain boundary and microstructural features have been demonstrated to strongly affect carriers scattering in other thermoelectric materials \(^\text{27}\). Compared to other common high-performance thermoelectric oxides, these values of resistivity are still high; other oxides like Ca$_3$Co$_4$O$_9$ \(^\text{28}\) prepared by conventional sintering, displays $3 \cdot 10^{-4} \, \Omega \, m$ in the whole temperature range of 300 - 973 K and polycrystalline NaCo$_2$O$_4$ \(^\text{20}\) samples have shown values of $4 \cdot 10^{-4} \, \Omega \, m$ at 730 K. A great improvement of the electrical resistivity is observed in the Pb doped derivative Bi$_{1.9}$Pb$_{0.1}$PdO$_4$, which is reduced down to $10^{-3} \, \Omega \, m$ at 700 K. This enormous reduction of three orders of magnitude could be attributed both, to the increased carrier concentration due to the hole-doping effect induced when Pb partially replaces Bi, and to the shorter metal-metal (Pd-Pd) distances, for which an increased overlap would yield broader bandwidth and an enhanced conductive path with increased carrier mobilities.

The Seebeck coefficient variation is shown in Figure 5a. Measurements of Bi$_2$PdO$_4$ exhibit a p-type behaviour with extremely high values from 1458 $\mu$V K$^{-1}$ at 340 K to 1218 $\mu$V K$^{-1}$ at 720 K, in agreement with the localized $d_{z^2}$ flat valence band in the $ab$ plane and large band degeneracy near the Fermi level \(^\text{16}\). The evolution with temperature is almost invariable up to 550 K, point at which the Seebeck coefficient starts to diminish due to the thermal excitation of minority carriers. The predicted Seebeck coefficient\(^\text{16}\)
follows a similar invariant trend and displays values close to 650 μV K⁻¹ for a carrier concentration of 10¹⁸ cm⁻³, which along with the resistivity values, suggest that the carrier concentration in our undoped samples is much lower and that other factors, such as grain boundaries, are playing an important role in the transport properties. These great values of the Seebeck coefficient provide room for optimization of the carrier concentration and its fine-tuning in relation to the electrical resistivity, as other oxides displays much lower values in the range 60 – 100 μV K⁻¹, as described for polycrystalline Bi₂Sr₂Co₂O₉ ²⁹ in the 300 – 1000 K temperature interval, or between 130 and 180 μV K⁻¹ measured in Ca₃Co₄O₉ ²⁸ at 300 – 973 K. Such is the case, that Pb doping reduces the Seebeck coefficient to the range of 200 μV K⁻¹, still in the range of good oxide thermoelectric materials values, and predicted for carrier concentrations between 5x10¹⁹ cm⁻³ and 10²⁰ cm⁻³ ¹⁶.

The power factor, S²σ of the undoped compound (Figure 5b), increases with temperature up to a maximum of 0.8 μW m⁻¹ K⁻², resulting from the electrical resistivity variation and an almost constant Seebeck coefficient. These values are below those found by the theoretical predictions ¹⁶, as a consequence of the higher electrical resistivity. As mentioned, the large Seebeck coefficient offers wide room for tuning through the optimization of the carrier concentration, as experimentally realized in Bi₁.₀Pb₀.₁PdO₄. Its enhanced resistivity improves the power factor up to 10 μW m⁻¹ K⁻². This huge enhancement by only one first attempt supports the promising predictions by theoretical calculations, and suggest that a synergistic improvement of Seebeck coefficient and electrical conductivity could be achieved by further doping strategies or new sample elaboration that diminish the scattering of charge carriers.

**Figure 5.** Temperature dependence of (left) Seebeck Coefficient and resistivity, and (right) power factor of pristine Bi₂PdO₄ (dark colours) and Bi₁.₀Pb₀.₁PdO₄ (light colours).
Thermal diffusivity ($\alpha$) of the samples was measured in a Linseis LFA instrument in the temperature range of 300 – 800 K by the laser-flash method. The surfaces of the pellets were covered with a thin graphite coating to maximize full emissivity from the backside and absorption at the front surface. The total thermal conductivity is calculated by $\kappa = \alpha C_p d$, where $C_p = 297$ J Kg$^{-1}$ K$^{-1}$ is the specific heat, determined by means of the Dulong-Petit approximation 30, and $d$ is the sample density. The thermal conductivity of the pristine and doped samples (Figure 6a) reflect the lattice conductivity, as the electronic contribution can be neglected due to high resistivity. A monotonous decrease is observed throughout the temperature range. Bi$_2$PdO$_4$ displays a maximum value of 3.3 W m$^{-1}$ K$^{-1}$ at 300 K down to 1.45 W m$^{-1}$ K$^{-1}$ at 823 K, being significantly lower compared to those measured in other oxide thermoelectric materials, as Ca$_3$Co$_4$O$_9$ and NaCo$_2$O$_4$, which show values around 2.0 – 4.0 W m$^{-1}$ K$^{-1}$ in this temperature range, and in fact, close to those previously described by the theoretical work of J. He et al. 16. The main source of this low lattice thermal conductivity is the structural distortion produced by the lone electron pair of Bi (Figure 6), and the related strong anharmonicity and distortion of the octahedral framework. Large isotropic displacement parameters found in Bi and O positions, and therefore, strong vibrations, have an important impact on the low thermal conductivity, which is in agreement with the theoretical study 16. Moreover, the Pb-doped sample display even lower values as 1.1 W m$^{-1}$ K$^{-1}$ at 823 K, which could be ascribed to the disorder produced upon doping, as suggested in the SXRD section. Additionally, the lattice thermal conductivity of the Pb-doped and the undoped samples was analyzed in terms of the Callaway model 32, 33 by considering three scattering mechanisms. Therefore, the model includes boundary scattering, point defects scattering and the Umklapp phonon-phonon scattering. Whereas the grain boundary term and the Umklapp scattering term show a similar trend for both samples, the point defect scattering term is markedly larger for the Pb-doped sample as we expected. The results of the calculated lattice thermal conductivity are included in figure 6a. Still, it would be possible to improve the thermoelectric efficiency of this material by further reduction of the lattice conductivity using other approaches as nanostructuration.

The Figure of Merit is plotted against temperature in Figure 6b. These values follow the same trend as the power factor, increasing throughout the temperature range up to 4x10$^{-4}$ at 680 K for the undoped Bi$_2$PdO$_4$ and to 6x10$^{-3}$ at 720 K for Bi$_{1.9}$Pb$_{0.1}$PdO$_4$. It is noteworthy the large thermopower of the pristine compound, consequence of a large band degeneracy and DOS, being a good starting point for the optimization of the thermoelectric performance. As a prove of concept, the figure of merit is largely enhanced by Pb doping due to the combination of electrical and thermal transport improvements, highlighting Bi$_2$PdO$_4$ and its derivatives as promising thermoelectric materials.
Figure 6. Temperature dependence of (left) Measured thermal conductivity, the dashed lines are the fits to Callaways’s model (see text), and (right) Figure of Merit of pristine Bi$_2$PdO$_4$ and Bi$_{1.9}$Pb$_{0.1}$PdO$_4$. The inset corresponds to a zoom-in on the undoped values.

Conclusions

The predictions of good thermoelectric coefficients in Bi$_2$PdO$_4$ have been realized in a polycrystalline sample prepared by solid-state reactions, yielding maximum $S=1458 \, \mu$V K$^{-1}$ at 340 K. The poor electronic conductivity is overcome in a Pd-doped sample, achieving better conductivities by three orders of magnitude, and an improved power factor up to $10 \, \mu$W m$^{-1}$ K$^{-2}$. An excellent correlation between crystal structure and properties has been established from high angular resolution SXRD data: the collapse of the unit cell along c-direction upon Pb doping, opposite to the expected from steric considerations, accounts for an increment of the charge carriers density, associated with the shorter Pd-Pd distances, presumably involving direct metal-metal bonds. The synchrotron diffraction data also permit the localization of the Bi electron lone pairs, at approximate distances of a Bi-O bond. The presence of lone electron pairs are responsible for the extremely distorted BiO$_6$ coordination environment, and correlated to a low thermal conductivity, better than that usually displayed by thermoelectric oxides. This parameter is even reduced upon Pb-doping as a consequence of the introduced structural disorder, and ascribed to anharmonicity of the chemical bonds. Therefore, Bi$_2$PdO$_4$ and doped derivatives can be auspicious as thermoelectric materials, since the transport properties are still susceptible of significant improvements.
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Experimental corroboration of the thermoelectric performance of Bi$_2$PdO$_4$ oxide and Pb- doped derivatives

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Predicted thermoelectric behaviour in Bi$_2$PdO$_4$ is experimentally realized. Pb doping enhances the power factor, with additional reduction of thermal conductivity.