Isotope selective photodissociation of N$_2$ by the interstellar radiation field and cosmic rays

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ABSTRACT

Context. Photodissociation of $^{14}$N$_2$, and $^{14}$N$^{15}$N occurs in interstellar clouds, circumstellar envelopes, protoplanetary discs, and other environments due to ultraviolet radiation originating from stellar sources and the presence of cosmic rays. This source of N atoms initiates the formation of more complex N-bearing species and may influence their isotopic composition.

Aims. To study the photodissociation rates of $^{14}$N$_2$ by ultraviolet continuum radiation and both isotopologues in a field of cosmic ray induced photons. To determine the effect of these on the isotopic composition of more complex molecules.

Methods. High-resolution theoretical photodissociation cross sections of N$_2$ are used from an accurate and comprehensive quantum-mechanical model of the molecule based on laboratory experiments, as presented for $^{14}$N$_2$, Li et al. 2013. A similarly high-resolution spectrum of H$_2$ emission following interactions with cosmic rays has been constructed. The spectroscopic data are used to calculate photodissociation rates which are then input into isotope-differentiated chemical models, describing an interstellar cloud and a protoplanetary disc.

Results. The photodissociation rate of $^{14}$N$^{15}$N in a Draine field assuming 30 K excitation is $1.73 \times 10^{-10}$ s$^{-1}$, within 4% of the rate for $^{14}$N$_2$, and the rate due to cosmic ray induced photons assuming an H$_2$ ionisation rate of $\zeta = 10^{-16}$ s$^{-1}$ is about $10^{-15}$ s$^{-1}$, with up to a factor of 10 difference between isotopologues. Shielding functions for $^{14}$N$^{15}$N by $^{14}$N$_2$, H$_2$, and H are presented. Incorporating these into an interstellar cloud model, an enhancement of the atomic $^{15}$N/$^{14}$N ratio over the elemental value is obtained due to the self-shielding of external radiation at an extinction of about 1.5 mag. This effect is larger when assumed grain growth has reduced the opacity of dust to ultraviolet radiation. The transfer of photolytic isotopic fractionation of N and N$_2$ to other molecules is demonstrated to be significant in a protoplanetary disc model with grain growth, and is species dependent with $^{15}$N enrichment approaching a factor of 10 for HCN. The cosmic ray induced dissociation of CO is revisited employing a more recent photodissociation cross section, leading to a rate that is ~40% lower than previously calculated.

Key words. molecules – cosmic rays – molecular processes – radiation mechanisms: non-thermal – photo-dominated region – protoplanetary discs

1. Introduction

Nitrogen is the fifth most abundance element in the universe and comprises two isotopes with relative populations $^{14}$N/$^{15}$N $\approx$ 400. The dominant reservoir of elemental N is in the form of atoms and N$_2$, which are essentially unobservable outside of the solar system, the former because its ionic form, N$^+$, is readily removed by charge exchange with neutral hydrogen with the latter lacking a rotational emission spectrum because it is homonuclear. The observation of electronic transitions of N$_2$ is limited to technologically-challenging ultraviolet (UV) wavelengths shorter than 1000 Å.

There have been numerous detections of N-derived molecules such as N$_2$H$^+$, CN, HCN, and NH$_3$ in interstellar space, protostellar envelopes and discs, and extra-galactically, (e.g. van Zadelhoff et al. 2001; Bergin et al. 2002; Gerin et al. 2009; Oberg et al. 2010; Tobin et al. 2012), as well as for their isotopologues (e.g. Wannier et al. 1991; Gerin et al. 2009; Adande & Ziurys 2012; Hily-Blant et al. 2013; Bizzocchi et al. 2013; Daniel et al. 2013). The balance of chemically active N and highly stable N$_2$ is an important parameter in the chemistry of these more complex amines and nitriles. The primary driver of this balance in environments exposed to an ultraviolet flux is photodissociation of N$_2$.

The value of $^{14}$N/$^{15}$N in observable species constitutes an astronomical puzzle. The solar elemental ratio, 440 (Marty et al. 2010), is considered representative of the local interstellar medium, but differs from the terrestrial value, 270; in the atmosphere of Titan, 180 (Niemann et al. 2005); and in interplanetary dust, meteorites and comets, 68–330 (Floss et al. 2006; Jehin et al. 2009; Alleon 2010; Mumma & Charnley 2011). Observational surveys have been made of galactic star-forming regions (Adande & Ziurys 2012) and dark clouds (Hily-Blant et al. 2013) and also point to a range of values, as well as variations by source and the molecular species observed. Some variation of $^{14}$N/$^{15}$N is clearly due to the details of local nuclear syn-
thesis, with an increasing excess of $^{15}$N towards the galactic centre (Wilson 1999; Adande & Ziurys 2012). Another proposed explanation for the observed ratios of $^{13}$C/$^{12}$C, $^{15}$N/$^{14}$N, and $^{14}$NH$_3$/$^{15}$NH$_3$ is low-temperature isotopic-exchange chemistry. Models considering this mechanism (e.g., Rodgers & Charnley 2008; Wirström et al. 2012; Le Gal et al. 2013) have been successful in introducing strongly non-elemental abundance ratios under specific conditions. The critical exchange reactions, e.g.,

$$\text{HC}^{14}\text{NH}^+ + ^{15}\text{N} \approx \text{HC}^{15}\text{NH}^+ + ^{14}\text{N} + \text{energy},$$

rely on the lower zero-point energy of the heavier molecular species and are exothermic by $\leq 30\,\text{K}$ (Terzieva & Herbst 2000), limiting their significance to cold environments. This is in contrast to similar reactions affecting the $\text{H}/\text{D}$ abundance in molecules which may proceed at temperatures as high as 170 K.

An alternative route to the mass fractionation of molecules is isotope selective photodissociation. For the case of $\text{N}_2$ dissociation, self-shielding has been shown to drive the $^{14}\text{N}^2\text{H}/^{14}\text{N}^2\text{H}$ ratio in the atmosphere of Titan (Liang et al. 2007). Additionally, there is strong observational evidence that the fractionation of protostellar oxygen isotopes is assisted by the self-shielding of CO, which has very similar molecular structure to $\text{N}_2$ (Shaffer et al. 2002; Lyons & Young 2005; Smith et al. 2009). The investigation of isotope selective $\text{N}_2$ photodissociation in interstellar clouds and protoplanetary environments is then highly warranted.

The importance of photodissociation due to the interstellar radiation field (ISRF) or an ultraviolet emitting star will decrease as the radiation is attenuated below the surface of an interstellar cloud, circumstellar envelope, or protoplanetary disc. Li et al. (2013) made a detailed assessment of the dissociation rate of $^{14}\text{N}_2$ and the shielding of ultraviolet radiation by relevant materials ($\text{H}_2$, $\text{H}^+$, $^{14}\text{N}_2$, itself, and dust grains). This work considered in detail the sharply structured absorption spectrum of $\text{N}_2$ and shielding species. This was made possible by means of an accurate and comprehensive quantum-mechanical model of $\text{N}_2$ photoabsorption and dissociation, which was informed by an extensive history of $\text{N}_2$ spectroscopy in the laboratory (e.g., Ajello et al. 1989; Helm et al. 1993; Sprangers et al. 2003, 2004, 2005a; Stark et al. 2008; Lewis et al. 2008b; Heays et al. 2009, 2011) and theoretically (e.g., Spelsberg & Meyer 2001; Lewis et al. 2005b; Haverd et al. 2005; Lewis et al. 2008a–c; Ndome et al. 2009). This model, detailed in Sec. 2, explicitly accounts for the nuclear masses and so is equally applicable to the case of $^{15}\text{N}_2$. In Sec. 3 of this paper, we describe new calculations of $^{14}\text{N}^{15}\text{N}$ photodissociation rates in interstellar and blackbody radiation fields.

The interior regions of interstellar clouds and protoplanetary discs may be completely shielded from external sources of ultraviolet photons. However, collisions between high-energy cosmic rays and $\text{H}_2$ produce a weak local UV field that could be important for photodissociation. The cosmic ray induced photoionisation and photodissociation of molecular and atomic species is well established (Greuel et al. 1987, 1989; Dalgarno 2006; Padovani et al. 2009). In Sec. 4 we combine our model of $\text{N}_2$ photoabsorption with a similarly thorough theoretical treatment of the $\text{H}_2$ line emission associated with cosmic rays. This is, to study in detail for the first time the photodissociation of $^{14}\text{N}_2$ and $^{14}\text{N}^{15}\text{N}_2$ in cloud and disc interiors. We also revisit calculations of the CO dissociation rate due to cosmic rays (Greuel et al. 1987) taking advantage of an updated photodissociation cross section.

In Sec. 5 of this paper we present the results of chemical models of an interstellar cloud and protoplanetary disc. These include linked chemical networks for species containing $^{14}\text{N}$ and $^{15}\text{N}$ and the photodissociation rates of Li et al. (2013) and Secs. 3 and 4. Using these models we investigate the consequences of isotope selective photodissociation on the abundances of atomic and molecular nitrogen and other $\text{N}$-bearing species observed in clouds and discs.

2. The model of photoabsorption and photodissociation

The photodissociation of $\text{N}_2$ first requires excitation into bound states that then rapidly predissociate. Thus, the photoabsorption spectrum contains well separated electronic-rovibrational lines and must be treated at high resolution ($\approx 10^{-3}$ Å) but over a comparatively large wavelength range (912–1000 Å). Actually, $\text{N}_2$ absorbs strongly at considerably shorter wavelengths but the present application is limited to longwards of the atomic $\text{H}$ ionisation threshold at 912 Å. Here, a broadband and detailed spectrum is calculated by means of a quantum mechanical model which solves a coupled Schrödinger equation (CSE) for the vibrational wavefunction of the molecule. Properties of the electronic wavefunction are described by potential-energy curves and state coupling parameters optimised with respect to a large database of laboratory line positions, oscillator strengths, and predissociation rates. These empirical parts of the CSE model formulation are independent of molecular mass, and so are unchanged by isotopic substitution of one or both nuclei. Then, the explicit calculation of vibrational wavefunctions models the quantum mixing of electronic states and its dependence on the nuclear masses. A more detailed description of the method, the important electronic states and potential-energy curves used in the model is given in our previous publication (Li et al. 2013), and the chemical physics literature (Lewis et al. 2005b; Haverd et al. 2005; Lewis et al. 2008a; Heays et al. 2011) with specific discussion of $^{15}\text{N}^{15}\text{N}$ given in Vieitez et al. (2008) and Heays et al. (2011).

Electric-dipole-allowed photoabsorption from the ground state occurs for wavelengths shorter than 1000 Å and accesses two valence states and several Rydberg series of $^3\Pi$, $^1\Pi$, and $^3\Sigma$ symmetry. Potential-energy curves depicting these states are shown in Fig. 1 with the lowest-energy photoabsorbing state, $^3\Pi_{3/2}$, occurring at 12.6 eV. There is strong electronic coupling between valence and Rydberg states of the same symmetry which leads to a very perturbed spectrum, including constructive and destructive interference in the absorption strength and predissociation rates of vibrational bands (Dressier 1969; Spelsberg & Meyer 2001; Lewis et al. 2005b). Additional rotational interactions between $^3\Pi_{1/2}$ and $^3\Sigma_{1/2}$ states lead to strong rotational dependence of line strengths and predissociation rates (or linewidths) (Stark et al. 2005; Heays et al. 2011).

Predissociation occurs through spin-orbit coupling of $^1\Pi$ states with a number of states with $^3\Sigma$ symmetry, including an unbound level, and one state of $^3\Sigma$ symmetry. These are shown in Fig. 1 and lead to dissociation into $\text{N}$ atoms in the $^4S$, $^2D$, or $^2P$ states. The spin-selection rules forbid the appearance of triplet states in optical spectra although many have been observed in the laboratory regardless, due to their coupling with $^3\Pi$ levels (Sprangers et al. 2005a; Lewis et al. 2008b). The majority of excited vibrational states predissociate after an absorption event with near certainty, that is, they have a predissociation fraction of $\approx 1$. For those states that decay substantially by emission, a reduction of the CSE-calculated photoabsorption cross section, $\sigma_{\text{abs}}$, has been made by their less-than-unitary predissociation.
Fig. 1. Diabatic-basis potential-energy curves of N$_2$ excited states relevant to ultraviolet photoabsorption and photodissociation. The energy scale is referenced to $v = 0$, $J = 0$ of the $X^1\Sigma^+_g$ ground state and is related to the wavelength scale assuming transitions from this fundamental level. Also indicated are the excitation states of atomic products arising from dissociation and the absorption limit imposed by the ionisation of atomic H. The potential-energy curves of the $\sigma$ and $\pi$ states are indistinguishable at the plotted scale. The N$_2$ ionisation potential energy occurs at 15.4 eV in this figure.

Fig. 2. An example of isotopically-dependent predissociation. The predissociation fraction, $\eta_{pd}$, of individual rotational levels, $J$, of $b^1\Pi_u (v = 1)$ calculated for $^{14}$N$_2$ and $^{15}$N$_2$.

3. Photodissociation rates and shielding functions

The photodissociation rate, $k_0$, of N$_2$ exposed to UV radiation can be calculated according to

$$k_0 = \int \sigma_{pd}(\lambda)I(\lambda)d\lambda,$$

where $\sigma_{pd}(\lambda)$ is the wavelength-dependent cross-section of $b^1\Pi_u (v = 1)$, or $b^1\Pi_u (v = 0)$, and $I(\lambda)$ is the wavelength-dependent intensity of incoming photons.

This provides an example of the utility of the physically-based CSE model. That is, the $b^1\Pi_u (v = 1)$ level of $^{14}$N$_2$ is known to predissociate significantly less rapidly than for $^{15}$N$_2$ (Sprengers et al. 2004, 2005b; Wu et al. 2012) because of mass-change-induced shifts of the interacting $^1\Pi_u$ and $^1\Pi_u$ levels. These shifts are evaluated explicitly by the CSE model and calculated predissociation fractions for $b^1\Pi_u (v = 1)$ are shown in Fig. 2 for rotational levels with angular momentum quantum number, $J \leq 30$. There is a strong dependence on rotational angular momentum, $J$, for both isotopologues. At the low temperatures of interstellar space only rotational levels with $J < 10$ are accessible. Then, photons absorbed by $^{15}$N$_2$ and leading to excitation of the $b^1\Pi_u (v = 1)$ level are nearly twice as likely to lead to a dissociation event than for $^{14}$N$_2$.

We have calculated $^{15}$N$_2$ photoabsorption and photodissociation cross sections as Li et al. (2013) did for $^{14}$N$_2$. A comparison is made in Fig. 3 between transmission functions derived from the two CSE-calculated photoabsorption cross sections. The principal difference is a shift of $^{15}$N$_2$ absorption bands to longer wavelengths which mostly increases with vibrational excitation, that is, with shortening wavelength. However, there are many further differences between the spectra of different N$_2$ isotopologues due to the strong coupling between excited states, such as depicted in Fig. 2 with respect to the $b^1\Pi_u (v = 1)$ predissociation fraction, and these should not be neglected (e.g., Viète et al. 2008; Lewis et al. 2008b; Heays et al. 2011).

The wavelengths of the majority of the modelled rovibrational lines are accurate to within 0.01Å when compared with laboratory measurements (Heays 2011). The magnitudes of the calculated cross sections are accurate to about 10%, with their principal uncertainty arising from the absolute calibration of the laboratory absorption oscillator strengths used to constrain the model electronic transition moments (Stark et al. 2005, 2008; Heays et al. 2009). The predissociation fractions pertaining to the longest wavelength bands are well known and modelled (Lewis et al. 2005b) but are less certain at shorter wavelengths. For these, a predissociation fraction of 1 is assumed. This is a reliable assumption with respect to $^1\Pi_u$ states, many of which are known to exhibit significant predissociation broadening (Stark et al. 2008; Heays et al. 2011). It is less certain that all $^1\Sigma^+_u$ levels responsible for absorption at shorter wavelengths are completely predissociative. Further practical details regarding the calculation of N$_2$ cross sections and dissociation fractions at different temperatures may be found in Li et al. (2013).

Also shown in Fig. 3 are transmission functions representing further line-absorbing species relevant to the following treatment of the shielding of N$_2$ absorption in astrophysical environments. For these, photoabsorption cross sections for H$_2$ are synthesised from data obtained from the Meudon PDR code website (Le Petit et al. 2006), and those for CO are taken from the model of Visser et al. (2009).
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\[ o-H_2:p-H_2 = 3:1 \quad o-H_2:p-H_2 = 0:1 \]

\[ H_2 \quad \text{Transmission} \]

\[ 915 \quad 920 \quad 925 \quad 930 \]

\[ H_2 \quad \text{emission} \]

\[ 0.0 \quad 0.2 \quad 0.4 \quad 0.6 \quad 0.8 \quad 1.0 \]

\[ \text{Transmission} \]

\[ 935 \quad 940 \quad 945 \quad 950 \quad 955 \]

\[ H_2 \quad \text{emission} \]

\[ 0.0 \quad 0.2 \quad 0.4 \quad 0.6 \quad 0.8 \quad 1.0 \]

\[ \text{Transmission} \]

\[ 960 \quad 965 \quad 970 \quad 975 \]

\[ H_2 \quad \text{emission} \]

\[ 0.0 \quad 0.2 \quad 0.4 \quad 0.6 \quad 0.8 \quad 1.0 \]

\[ \text{Transmission} \]

\[ 980 \quad 985 \quad 990 \quad 995 \quad 1000 \]

\[ \text{Wavelength (Å)} \]

Fig. 3. Upper subfigures: Representative transmission functions calculated from theoretical photoabsorption cross sections of important molecular species, with column densities: \( N(H) = 10^{22}, N(H_2) = 10^{20}, \) and \( N(^{14}\text{N}_2) = N(^{14}\text{N}^{15}\text{N}) = N(\text{CO}) = 10^{15} \text{cm}^{-2}; \) and simulating an excitation temperature of 50 K for all molecular absorption. Lower subfigures: Probability per Å of H₂ emission following a cosmic-ray induced ionisation event. Spectra are shown assuming two different values for the H₂ ortho:para ratio.

where \( \sigma^{\text{pd}}(\lambda) \) is the N₂ photodissociation cross section described in Sec. 2, \( I \) is the intensity of the radiation field, and \( \lambda \) the wavelength. The unattenuated interstellar radiation field (ISRF) of Draine (1978), in units of photons \( \text{cm}^{-2} \text{s}^{-1} \text{Å}^{-1} \text{sr}^{-1} \), is used in most of the following calculations and is given by

\[
F(\lambda) = \frac{1}{4\pi} \left( 3.2028 \times 10^{15} \lambda^{-3} - 5.1542 \times 10^{18} \lambda^{-4} + 2.0546 \times 10^{21} \lambda^{-5} \right).
\]
Table 1. The unattenuated photodissociation rates \((k_0, \text{s}^{-1})\) of \(\text{N}_2\) exposed to a completely-surrounding Draine interstellar radiation field for various excitation temperatures \((T_{ex})\), and for blackbody radiation with temperature \(T_{bb}\) and \(T_{ex} = 30\) K.

| \(T_{ex}(\text{K})\) | \(14\text{N}_2\) | \(14\text{N}^{15}\text{N}\) |
|-----------------|-----------------|------------------|
| 10              | \(1.64 \times 10^{-10}\) | \(1.68 \times 10^{-10}\) |
| 20              | \(1.65 \times 10^{-10}\) | \(1.70 \times 10^{-10}\) |
| 30              | \(1.66 \times 10^{-10}\) | \(1.71 \times 10^{-10}\) |
| 50              | \(1.67 \times 10^{-10}\) | \(1.72 \times 10^{-10}\) |
| 100             | \(1.70 \times 10^{-10}\) | \(1.74 \times 10^{-10}\) |
| 1000            | \(1.79 \times 10^{-10}\) | \(1.87 \times 10^{-10}\) |

Notes. (a) The integrated energy intensities of all radiation fields over the interval 912–2050 Å have been normalised to \(\chi = 1\) Draine [1978] field.

with \(\lambda\) in Å. In the following we employ an angle-integrated intensity,

\[ I(\lambda) = 4\pi\chi F(\lambda), \]

with an additional scaling factor relative to the Draine field, \(\chi\). The integral in Eq. (2) must be computed between 912 and 1000 Å. This range is defined by the long-wavelength onset of the \(\text{N}_2\) absorption spectrum and the complete suppression of ultraviolet radiation for wavelengths shorter than the atomic H ionisation limit.

The photodissociation rates of \(14\text{N}_2\) and \(14\text{N}^{15}\text{N}\) calculated from Eq. (2) are given in Tab. 1 assuming several different radiation fields. In all cases the difference between \(14\text{N}_2\) and \(14\text{N}^{15}\text{N}\) rates is below 5%, and the calculated dependences on the \(\text{N}_2\) ground state excitation temperature and the form of the incident field (a Draine ISRF, or blackbody radiation) are similar to those calculated by Li et al. [2013] for \(14\text{N}_2\).

For \(\text{N}_2\) embedded in an externally irradiated cloud or disc, the intervening gaseous and granular material acts as a shield and leads to a reduced photodissociation rate, \(k < k_0\). The precise nature of shielding by H, H\(_2\), \(14\text{N}_2\), and \(14\text{N}^{15}\text{N}\) is influenced by the wavelength dependence of their absorption cross sections, but is more usefully applied as a wavelength-integrated ratio of shielded and unshielded dissociation rates. That is, the shielding function given by

\[ \theta = \frac{k}{k_0} = \frac{\int I(\lambda) \exp \left[ -\sum X N_X \sigma_{\text{abs}}(\lambda) \right] \exp (-\gamma_{\text{dust}} A_V) \sigma_{\text{pl}}(\lambda) d\lambda}{\int I(\lambda) \sigma_{\text{pl}}(\lambda) d\lambda} \]

(5)

Here, \(\sigma_{\text{abs}}(\lambda)\), is the absorption cross section of shielding species X and \(N_X\) its shielding column density.

The term \(\exp (-\gamma_{\text{dust}} A_V)\) in Eq. (5) describes shielding of the UV flux by dust grains, where the visual (5500 Å) extinction is assumed proportional to the column density of hydrogen nuclei, \(N_\text{H}\), according to \(A_V = N_\text{H}/1.6 \times 10^{21}\) [Savage et al. [1977]]. In principle, this is a wavelength dependent quantity which depends on the distribution of dust grain sizes, their composition, and their geometries. The use of a simple parameterisation of declining intensity with increasing visual extinction is warranted by the significant uncertainties in these parameters. Radiative transfer calculations considering the destruction and scattering of photons by a realistic distribution of interstellar dust grains were made by Roberge et al. [1981] and [1991]. The ultraviolet extinction relevant to various molecules was parameterised by van Dishoeck et al. [2006] as a decaying exponential like that in Eq. (5) using the dust optical properties of [Roberge et al. 1991]. Their extinction calculated for the wavelength range appropriate to CO is adopted here for \(\text{N}_2\), that is with \(\gamma_{\text{dust}} = 3.53\). Further calculations were made by van Dishoeck et al. [2006] assuming larger dust grains (> 1μm in size) as identified in protoplanetary discs (Li & Lunine 2003b; Jonkheid et al. 2006). For this case \(\gamma_{\text{dust}} = 0.6\).

Detailed shielding functions for \(14\text{N}_2\) were given in Li et al. [2013] and the associated on-line material. Here, new calculations are made for \(14\text{N}^{15}\text{N}\) using Eq. (5), with some representative results plotted in Fig. 4 and full details available from the Draine photodissociation database [1]. The data in Fig. 4 assume that the lines of shielding H and H\(_2\) are Doppler broadened by \(\sigma = 1\) and 3 km s\(^{-1}\) respectively. The \(\text{N}_2\) lines are assigned thermal Doppler widths according to their excitation temperatures but are also naturally broadened by the predissociation process, in some cases by a few km s\(^{-1}\).

Unsurprisingly, the similarity of the two isotopologues leads to very similar shielding functions. There is some difference evident in Fig. 4 with respect to shielding by atomic hydrogen. That is, the shielding of \(14\text{N}^{15}\text{N}\) by a N(H) = 10\(^{14}\) cm\(^{-2}\) column is somewhat more effective than for \(14\text{N}_2\). This is the result of a nearer alignment of the \(b^1\Pi_g(v = 3) \leftrightarrow X^1\Sigma_g^+(v'' = 0)\) absorption band of \(14\text{N}_2\) and the line-centre of the shielding \(4p \leftrightarrow 1s\) transition of atomic hydrogen. The relevant \(14\text{N}_2\), \(14\text{N}^{15}\text{N}\), and H features are plotted in Fig. 3 near 972 Å. For a larger H column, like that in Fig. 3 with heavily saturated and broadened H lines, the misalignment of H and \(14\text{N}_2\) transitions near 972 Å loses its significance.

Also shown in Fig. 4 is the shielding of \(14\text{N}^{15}\text{N}\) photodissociation by \(14\text{N}_2\). This rivals \(14\text{N}^{15}\text{N}\) self-shielding because of the much greater abundance of \(14\text{N}_2\). This is particularly true at higher temperatures where the wavelength offset between isotopologues is compensated for by their broader rotational distributions and Doppler widths. A discussion of the relative importance of different species in mixed shielding media is given in Sec. 5 with respect to an example protoplanetary disc.

Shielding functions calculated according to Eq. (5) describe the reduction in photodissociation rate due to the attenuation of unidirectional radiation. A related quantity, \(\theta_{\text{dust}}(N)\), describes this reduction as a function of column density for an extended medium illuminated isotropically at its surface. The resultant non-perpendicular rays penetrate less deeply and \(\theta_{\text{dust}}(N)\) is smaller than the shielding function in the unidirectional case, \(\theta(N)\) (Rollig et al. 2007). For a plane-parallel shielding medium with \(N\) defined perpendicular to its surface, the two shielding

\[^{1}\text{www.strw.leidenuniv.nl/~ewine/photo}\]
functions are related geometrically by the formula
\[
\theta_{\text{tot}}(N) = \int_0^{\frac{\pi}{2}} \left( \frac{N}{\cos \phi} \right) \sin \phi \, d\phi. \tag{6}
\]

4. Photodissociation due to cosmic-rays

4.1. Cosmic-ray induced emission and photodissociation model

The ionisation of H\(_2\) by cosmic ray collisions leads to the generation of free electrons. These may collisionally excite (or ionise) further H\(_2\) whose radiative relaxation generates an ultraviolet flux (Prasad & Tarafdar 1983; Cecchi-Pestellini & Aiello 1992). Sternberg et al. (1987), Gredel et al. (1987), and Gredel et al. (1989) estimated the photodissociation properties of several small molecules due to ultraviolet photons arising from this process. Similar calculations are made here for the dissociation of N\(_2\) including the detailed effects of line absorption as modelled by the CSE dissociation cross sections.

The H\(_2\) emission flux between 912 and 1000 Å is dominated by line transitions. This emission occurs primarily through the Lyman and Werner bands connecting the ground state with the \(B^1\Sigma^+\) and \(C^1\Pi_u\) excited states (Sternberg et al. 1987), and with a smaller contribution arising from other excited states (Gredel et al. 1989). Here, we use a model simulating the excitation of 9 electronic states of H\(_2\) by cosmic-ray generated electrons and the resulting emission, developed and expounded in detail by Gredel et al. (1987) and Gredel et al. (1989). This model includes the effects of cascading from sufficiently high-energy states into \(B^1\Sigma^+_u\) and competing predissociative decay.

The final result of the H\(_2\) emission model is a spectrum, \(P(\lambda)\), describing the number of photons generated per unit spectral density per H\(_2\) ionisation event. A plot of \(P(\lambda)\) is shown in Fig. 3 and demonstrates a large number of narrow emission lines which actually occupy very little of the wavelength interval shown. The widths of these lines are Doppler limited and assigned full-width half-maxima of 0.005 Å, which is appropriate for a typical dark-cloud non-thermal Doppler broadening of \(b = 1 \, \text{km s}^{-1}\). This is comparable to the widths of N\(_2\) absorption lines, also shown in Fig. 3, so model spectra of both species are treated at similarly high resolution. Spectra are shown in Fig. 3 assuming limiting high- and low-temperature ratios for the ortho:para H\(_2\) popula-
tions, \(\alpha - \text{H}_2 : p - \text{H}_2 = 3 : 1\) and 0 : 1, respectively. The difference is quite apparent and is significant in the following calculations of \(N_2\) photodissociation. Despite the 170 K energy separation of \(\alpha - \text{H}_2\) and \(p - \text{H}_2\) ground-state levels it is not evident that their low-temperature equilibrium populations are always attained in real molecular clouds (Tielens 2013). Thus, we choose to contrast high and low temperature limits in the present study.

The rate of ultraviolet photons generated by cosmic ray collisions per unit spectral density per hydrogen nucleus is given by

\[
R(\lambda) = \zeta \chi_{\text{H}_2} P(\lambda), \tag{7}
\]

where \(\chi_{\text{H}_2} = n(\text{H}_2)/[n(\text{H}) + 2n(\text{H}_2)]\) is the relative abundance of molecular hydrogen with respect to H nuclei and \(\zeta\) is the cosmic-ray-induced ionisation rate per \(\text{H}_2\) molecule. A value of \(\zeta = 10^{-16}\) s\(^{-1}\) per \(\text{H}_2\) is adopted for the following calculations and falls within the broad range of rates estimated from observations of ions in diffuse and translucent clouds (Dalgarno 2006, Padovani et al. 2009, Indriolo & McCaill 2012, Rimmer et al. 2012). This collection of observations suggest a rate as high as \(10^{-15}\) s\(^{-1}\) at the edge of an interstellar cloud, which decreases with extinction to \(\sim 10^{-16}\) s\(^{-1}\) for \(A_V = 10\) mag as the lowest-energy cosmic rays are attenuated. Our adopted value is therefore observed in the interiors of the densest clouds with \(\zeta < 10^{-15}\) s\(^{-1}\) (Hezareh et al. 2008). Theoretical consideration of a range of source and attenuation mechanisms influencing the cosmic ray flux (Padovani et al. 2009, Cleeves et al. 2013) suggest a smaller rate \(\zeta\) than \(10^{-16}\) s\(^{-1}\) may be expected in circumstellar environments, because of the possible influence of any stellar wind and magnetic field. The photodissociation results presented here may be adapted to ionisation rates other than \(\zeta = 10^{-16}\) s\(^{-1}\) by a simple scaling.

The cosmic-ray generated photons may be absorbed by dust grains and by abundant line-absorbing species: \(\text{H}_2\), \(\text{H}\), \(\text{N}_2\), and CO. The idea of an absorbing column density is inappropriate because of the local nature of the photon source. Instead, the fraction of ultraviolet radiation absorbed by a particular species, \(X\), and leading to its dissociation is determined from its relative abundance \(x_X\), according to

\[
x_X(\lambda) = \chi_X \sigma_X^{\text{pd}}(\lambda) / \chi_{\text{dust}} \sigma_{\text{dust}} + \sum_i x_i \sigma_i^{\text{abs}}(\lambda), \tag{8}
\]

Here, \(\chi_X\) and \(\sigma_X^{\text{abs}}(\lambda)\) are the abundances and photoabsorption cross sections of various species, \(\chi_{\text{dust}} \sigma_{\text{dust}}\) represents dust absorption, and \(\sigma_X^{\text{pd}}(\lambda)\) is a photodissociation cross section.

An important term in the summation in Eq. (8) arises from \(\text{H}_2\). For the cases of \(X\) being \(^{14}\text{N}_2\) or CO, self-shielding is important and must also be included. Self-shielding and shielding by \(^{14}\text{N}_2\) are both important for the case of \(^{14}\text{N}_2^{15}\text{N}\) photodissociation. Atomic hydrogen is also a source of UV shielding at the edge of a cloud or disc but is assumed here to have too low abundance (about \(10^{-4}\) relative to \(\text{H}_2\)) to be important in fully shielded regions. Consequently, the common assumption that all radiation shortwards of 912 Å is completely consumed by H ionisation does not apply here. However, the \(N_2\) photodissociation cross section at shorter wavelengths and approaching the photoionisation limit at 800 Å contributes less than 10\% to its total photodissociation rate, and is neglected here.

Shielding of a penetrating interstellar radiation field by dust grains was discussed in Sec. 3. The extinction of cosmic-ray induced radiation is treated differently. In this case, all photons are assumed absorbed before traversing a significant fraction of the dark interior of the interstellar cloud or disk where they are generated. Then, the detailed angular scattering of photons by dust grains is inconsequential and only the absorption cross section need be considered. The dust absorption cross section is related to its extinction cross section by

\[
\sigma_{\text{dust}}^{\text{abs}} = \sigma_{\text{dust}}^{\text{ext}} (1 - \omega), \tag{9}
\]

where \(\omega\) is the grain albedo. We adopt a commonly used value derived from observations (Savage et al. 1977, Bohlin et al. 1978) for the dust extinction cross section per hydrogen nucleus of \(2 \times 10^{-21}\) cm\(^2\) and assume an albedo of \(\omega = 0.5\). Then, 

\[
\chi_{\text{dust}} \sigma_{\text{dust}}^{\text{abs}} = 10^{-21}\text{cm}^2\text{ in Eq. (8).}
\]

The assumption of locally-absorbed UV photons is only appropriate for a sufficiently large and homogeneous medium. The mean-free-path of cosmic-ray generated photons in an interstellar cloud of density \(n_H = 10^4\) cm\(^{-3}\) is 30,000 AU, assuming the UV-to-visible extinction factor of 3.53 discussed in Sec. 3. For the larger densities found near the midplane of a protoplanetary disc (Jonkheid et al. 2006) this distance is accordingly reduced, e.g., \(n_H = 10^{6}\) cm\(^{-3}\) and \(\sim 1\) AU. In principle, the various cosmic-ray induced photodissociation rates calculated below will be overestimated for objects which are not significantly larger than this mean-free-path, due to the escape of some UV photons. However, the significance of cosmic-ray induced photon fluxes is generally limited to regions fully-shielded from external UV radiation, and such regions also necessarily shield the escape of internally-generated photons.

The dust grains in a protoplanetary disc are likely larger than those in interstellar space, which have radii \(< 1\) µm (Mathis et al. 1977, Li & Lunine 2003a) deduced properties of the dust grains in one protoplanetary system, HD 4796A, by reference to observed infrared and sub-millimetre wavelength emission. Their modelling required a lower limit of 1 µm on the grain size distribution. The \(N_2\)-dissociating cosmic-ray induced UV flux considered here has wavelengths shorter than 1000 Å and will not be as strongly absorbed by grains larger than this. However, a population of polycyclic aromatic hydrocarbons (PAHs) has been inferred in a number of discs (e.g., Li & Lunine 2003a, Geers et al. 2006, 2007, Maaskant et al. 2013) and will absorb extra UV radiation (Sibbenmorgen & Krügel 2010). Choparro (2012) assumed a dust distribution with a minimum grain size of 0.1 µm in their study of cosmic-ray induced photodissociation in a model disc. Following from this assumption they deduced a value of \(\chi_{\text{dust}} \sigma_{\text{dust}}^{\text{abs}} = 1.47 \times 10^{-22}\text{ cm}^2\), significantly below the commonly-adopted interstellar value. Here, we explore an even lower value, \(\chi_{\text{dust}} \sigma_{\text{dust}}^{\text{abs}} = 10^{-23}\text{ cm}^2\), in order to contrast a more extreme case of grain growth in a protoplanetary disc with interplanetary dust.

Finally, the photodissociation rate of species \(X\) (per molecule \(X\)) due to cosmic ray induced photons may be calculated according to

\[
k_X = 1 / x_X \int R(\lambda) p_X(\lambda) \, d\lambda. \tag{10}
\]

In some previous descriptions of cosmic-ray induced photodissociation (Gredel et al. 1989, McElroy et al. 2013) an efficiency is defined by factoring the \(\text{H}_2\) ionisation rate and dust grain albedo from Eq. (10). In this case, the importance of molecular line absorption in Eq. (8) prevents the factoring of dust properties.
Table 2. Photodissociation rate per molecule due to cosmic-ray induced radiation.

| Dissociation rate (×10^{-16} s^{-1}): | ^{14}\text{N}_2 | ^{14}\text{N}^{15}\text{N} | CO |
|---|---|---|---|
| Base conditions for an interstellar cloud |
| $\zeta = 10^{-16}$ s^{-1} | $x_{\text{N}_2} = 10^{-5}$ | $x_{\text{N}_2/\text{N}_2} = x_{\text{N}_2/225}$ | $x_{\text{CO}} = 7 \times 10^{-5}$ |
| $T_{\text{ex}} = 20$ K | 14 | 21 | 8.1 |
| $b = 1$ km s^{-1} | $o-H_2:p-H_2 = 3:1$ | $x_{\text{H}_2\text{O}}^{\text{abs}} = 10^{-21}$ cm^{2} |
| Variations |
| $T_{\text{ex}} = 10$ K | 13 | 44 | 12 |
| $T_{\text{ex}} = 30$ K | 18 | 28 | 9.2 |
| $T_{\text{ex}} = 100$ K | 8.7 | 30 | 7.5 |
| $T_{\text{ex}} = 300$ K | 6.8 | 20 | 10 |
| $b = 3$ km s^{-1} | 17 | 11 | 9.1 |
| $b = 5$ km s^{-1} | 19 | 12 | 10 |
| $x_{\text{N}_2/\text{N}_2} = 10^{-5}$, $x_{\text{CO}} = 7 \times 10^{-5}$ | 47 | 36 | 54 |
| $x_{\text{N}_2/\text{N}_2} = 10^{-3}$, $x_{\text{CO}} = 7 \times 10^{-3}$ | 45 | 36 | 40 |
| $x_{\text{N}_2/\text{N}_2} = 10^{-2}$, $x_{\text{CO}} = 7 \times 10^{-2}$ | 33 | 33 | 21 |
| $x_{\text{N}_2/\text{N}_2} = 10^{-1}$, $x_{\text{CO}} = 7 \times 10^{-1}$ | 2.8 | 8.4 | 2.1 |
| $T_{\text{ex}} = 10$ K, $o-H_2:p-H_2 = 0:1$ | 8.0 | 6.6 | 8.0 |
| $T_{\text{ex}} = 20$ K, $o-H_2:p-H_2 = 0:1$ | 8.9 | 22 | 9.5 |
| $T_{\text{ex}} = 30$ K, $o-H_2:p-H_2 = 0:1$ | 9.2 | 42 | 10 |
| $x_{\text{N}_2/\text{N}_2} = x_{\text{N}_2/100}$ | – | 17 | – |
| $x_{\text{N}_2/\text{N}_2} = x_{\text{N}_2/50}$ | – | 14 | – |

Modification for a protoplanetary disc

$x_{\text{H}_2\text{O}}^{\text{abs}} = 10^{-21}$ cm^{2}

| $T_{\text{ex}} = 10$ K, $o-H_2:p-H_2 = 3:1$ | 18 | 69 | 19 |
| $T_{\text{ex}} = 20$ K, $o-H_2:p-H_2 = 3:1$ | 21 | 52 | 15 |
| $T_{\text{ex}} = 30$ K, $o-H_2:p-H_2 = 3:1$ | 23 | 75 | 16 |
| $T_{\text{ex}} = 10$ K, $o-H_2:p-H_2 = 0:1$ | 11 | 18 | 17 |
| $T_{\text{ex}} = 20$ K, $o-H_2:p-H_2 = 0:1$ | 12 | 62 | 18 |
| $T_{\text{ex}} = 30$ K, $o-H_2:p-H_2 = 0:1$ | 14 | 118 | 17 |

4.2. Cosmic-ray induced photodissociation of $^{14}\text{N}_2$

The rate of dissociation of $^{14}\text{N}_2$ and $^{14}\text{N}^{15}\text{N}$ due to cosmic-ray induced ultraviolet radiation has been calculated and listed in Tab. 2. This rate is dependent on the local physical conditions, and a set of base conditions is chosen which plausibly simulate the interior of a dark interstellar cloud:

- The assumed abundances of $^{14}\text{N}_2$ and CO relative to nH = n(H) + 2n(H_2) are 10^{-5} and 7 × 10^{-3}, respectively, and reflect typical dense cloud abundances (Aikawa et al. 2008).
- A $^{14}\text{N}_2 : ^{14}\text{N}^{15}\text{N}$ ratio of 225 is chosen, appropriate for the solar elemental ratio of 450 (Marty et al. 2010).

- All molecular species are assumed to have a thermal excitation of $T_{\text{ex}} = 20$ K and be turbulent broadened with Doppler velocity $b = 1$ km s^{-1}.
- Dust grains are assumed to have a scattering cross section per H nucleus of $x_{\text{H}_2\text{O}}^{\text{abs}} = 10^{-21}$ cm^{2}.
- The high temperature limit, 3:1, is assumed for the ortho/para ratio of emitting H_2.

Further calculations listed in Tab. 2 probe variations on this set of parameters.

For the base set of parameters considered in Tab. 2 the $^{14}\text{N}_2$ photodissociation rate is $14 \times 10^{-16}$ s^{-1}. This is 5 orders of magnitude below the rate calculated for a standard interstellar radiation field in Sec. 3. The cosmic-ray induced photodissociation rates calculated by (Gredel et al. 1989) for a large number of other molecular species are generally larger than the $^{14}\text{N}_2$ value determined here, in many cases by multiple orders of magnitude. For example, assuming $\zeta = 10^{-16}$ s^{-1} and a grain albedo of $\omega = 0.5$, their photodissociation rates for H_2O and CN are $2.0 \times 10^{-14}$ and $1.8 \times 10^{-13}$ s^{-1}, respectively.

The self-shielding of $^{14}\text{N}_2$ cannot be neglected because of the resonant nature of its spectrum. For this reason, decreasing the $^{14}\text{N}_2$ density rapidly increases the dissociation rate, until the abundance relative to H nuclei, $x_{\text{N}_2}$, falls below about 10^{-7}, as is evident from the values in Tab. 2. Line absorption of H_2 also effectively shields N_2 dissociation, reducing its rate by a factor of 2. Dust opacity reduces the $^{14}\text{N}_2$ dissociation rate by a further 35%, and shielding by CO less than 5%.

The effective dissociation of $^{14}\text{N}_2$ arises from relatively few overlaps between its absorption lines and H_2 emission lines. These are indicated by steps in an accumulation of the integrated dissociation rate with wavelength, as shown in Fig. 6. This accumulation is dominated by a line overlap occurring at 960.45 Å, plotted in detail in Fig. 5. This corresponds to the P(4) line of the $c_3 \Pi_u(v' = 0) \rightarrow X \Sigma_g^+(v'' = 0)$ absorption band of $^{14}\text{N}_2$ and the P(3) line of the $B \Sigma_u^+(v' = 13) \rightarrow X \Sigma_g^+(v'' = 0)$ H_2 Lyman emission band. The significance of this overlap is dependent on the assumed excitation temperatures of absorbing $^{14}\text{N}_2$ and shielding H_2. When $T_{\text{ex}} = 20$ K, as indicated in Figs. 5 and 6, the fraction of N_2 ground state molecules in the $J = 3$ rotational level is low and the significance of the 960.45 Å overlap is small. For $T_{\text{ex}} = 100$ K, the $J = 3$ level population of ground state H_2 becomes significant and P(3) absorption effectively shields $^{14}\text{N}_2$ photodissociation. Thus, the largest $^{14}\text{N}_2$ photodissociation rate occurs at intermediate temperature.

Only small increases in the $^{14}\text{N}_2$ photodissociation rate occur for increased turbulent broadening, b. Greater sensitivity is found with respect to the assumed $o-H_2:p-H_2$ ratio. This is limited to 0:1 and 3:1 at high and low temperatures, respectively, given sufficiently high densities for thermal equilibrium to be maintained. The $^{14}\text{N}_2$ photodissociation rate is approximately halved when the low temperature limit is adopted, primarily because the H_2 emission at 960.45 Å arises from an excited $o-H_2$ level.

Table 2 also includes photodissociation rates assuming reduced absorption by dust grains, in order to simulate the interior of a protoplanetary disc. The adopted value of $x_{\text{H}_2\text{O}}^{\text{abs}}$ effectively removes dust from the competitive absorption of photons. The N_2 photodissociation rate is then somewhat higher than for an interstellar cloud, but follows the same trends with respect to temperature and the $o-H_2:p-H_2$ ratio.

Calculations of the cosmic-ray induced photodissociation of $^{14}\text{N}^{15}\text{N}_2$ are also presented in Tab. 2. The resultant rate assuming
5. Chemical models including photodissociation

5.1. Interstellar cloud model

A chemical model simulating an interstellar cloud was studied in order to explore the details of $^{14}\text{N}^{15}\text{N}$ photodissociation due to an interstellar radiation field impinging on its surface and a flux of cosmic rays within its interior. The model is similar to that of Li et al. (2013). Here, we used a modified version of the UMIST 2012 chemical network (McElroy et al. 2013). The network was stripped down to species containing only H, He, C, N and O; and a maximum of two C, N or O atoms. Supra-thermal chemistry was included to enhance the formation of CH$^+$ (and thus also CO) at low $A_V$, following Visser et al. (2009). This
boosts the rate of ion-neutral reactions after setting the Alfvén speed to 3.3 km s⁻¹ for column densities less than 4 × 10²⁰ cm⁻².

Freeze-out and thermal evaporation for all neutral species were added to the gas-phase only UMIST network as well as the grain-surface hydrogenation reactions used by Visser et al. (2011). The latter include H₂ formation and the conversion of C to CH₂, N to NH₃, O to H₂O, and S to H₂S. Photodesorption due to the UV field generated from cosmic-ray ionisation and the attenuated ISRF were included, but direct cosmic-ray desorption was not.

The wavelength dependence of the Draine ISRF was adopted for a unidirectional radiation field perpendicularly incident on the model cloud’s edge. This was scaled by a factor of λ₁ = 1 so that one-sided irradiation of the cloud leads to the same unshielded dissociation rates at its edge as those given in Tab. 1. The cloud is assumed sufficiently thick that no radiation penetrates from the far side. Self-shielding of CO is computed using the shielding functions of Visser et al. (2009), for 14N₂, we use those calculated by Li et al. (2013) at 30 K, and the presently calculated shielding functions are used for 15N₂. The scattering of UV radiation out of the incident beam is not included in our model.

The wavelength dependence of the Draine ISRF was designed to simulate an isotropic field generated from a remote stellar population (Draine 1978), and some previous interstellar cloud models also assume isotropic radiation (Röllig et al. 2007). The transition between atomic and molecular H₂ was shown by Röllig et al. (2007) to differ between irradiation geometries, occurring at lower Aᵥ for the isotropic case relative to unidirectional radiation. The transition for N₂ occurring in our unidirectional model would be similarly shifted to shallower depth if the incident radiation were isotropic.

The elemental abundances relative to H are those of Aikawa et al. (2008): 0.0975 for He, 7.86 × 10⁻⁵ for C, 2.47 × 10⁻⁵ for N, and 1.80 × 10⁻⁴ for O. The elemental 14N:15N ratio was fixed to the protosolar value, 450:1. The rate of H₂ ionisation due to cosmic rays was set to 5 × 10⁻¹⁴ s⁻¹. The abundances of N, N₂ and CO reach steady state after ~1 Myr, regardless of whether the gas starts in atomic or molecular form.

The cloud was assumed to have a constant hydrogen-nuclei density of n_H = n(H) + 2n(H₂) = 10⁶ cm⁻³ and a temperature of 30 K. The turbulent broadening, b, of CO, H₂, and H were set to 0.3, 3, and 5 km s⁻¹; respectively; and N₂ lines were assigned linewidths equivalent to their thermal Doppler width at 30 K, in an identical fashion to the similar model of Li et al. (2013).

The dust population was assigned a coefficient v_dust = 3.53 in Eq. 5 to simulate grains with an interstellar size distribution, with radius ~0.1 μm size. A value for the cosmic-ray induced photodissociation rate of N₂ was adopted corresponding to the low temperature o-H₂:p-H₂ ratio, 0:1.

The nitrogen reaction network was augmented so that separate accounting of pure 14N and single-15N containing species was possible. For this, all N-containing species and reactions were cloned and a 14N to 15N substitution made. Two kinds of isotope-differentiating reactions are included in our model chemical network: photodissociation and low-temperature isomolecular exchange reactions. The selective effects of photodissociation are encoded in the shielding functions and cosmic-ray induced photodissociation rates presented in Secs. 3 and 4. Exchange reactions were added to our network using the rates listed in Tab. 2 of Terzieva & Herbst (2000). These reactions exothermically favour increased abundances of 15N in more complex species because of the lower zero-point energy of molecules with heavier nuclei, with typical excess energies of 10 to 30 K.

Figure 7 shows the calculated abundances of 14N, 15N, 14N₂, and 14N₁₅N as well as their accumulated column densities, i.e.,

\[ \text{Cumulative column density} = \int_0^{\infty} n(X)dz, \]

where n(X) is the absolute abundance of species X and z(Aᵥ) is the distance from the clouds edge for a particular extinction. The trend of these quantities as a function of Aᵥ is qualitatively very similar for either isotopologue. Nitrogen is preserved in atomic form near the edge of the cloud due to the intense photodissociating interstellar radiation field. Increasing shielding with depth into the cloud permits a significant population in molecular form beginning around Aᵥ = 1.5.

The relative abundances of 14N₁₅N and 14N₂₁₅N calculated by the model are shown in Fig. 7. Any fractionation process will alter the isotopic abundances from the assumed elemental ratios 14N₁₅N = 0.450 and 14N₂₁₅N = 0.225. There is indeed an enhancement of 14N in atomic form for Aᵥ between 1 and 3 mag, and its consequent depletion in the form of N₂. This range of extinction corresponds to a column-density of 14N₂ sufficienctly large to significantly self-shield the ISRF and slow its rate of photodissociation. The lower column of 14N₂ is not as effectively self-shielding and leads to a larger 14N₁₅N photodissociation rate and the calculated excess of 15N atoms.

A modified model was also run neglecting ion-molecule exchange reactions in order to test their contribution to the calculated fractionation. The modelled abundances were not significant altered by this modification and the fractionation between Aᵥ = 1 and 3 mag is completely dominated by isotope-selective photodissociation due to self-shielding, at least at the adopted temperature of 30 K. In contrast, significant enhancements of 15N in NH₃ and HCN were produced in the models.
Fig. 7. Top: Abundances relative to H nuclei and left-to-right accumulated column densities of the isotopologues of N and N$_2$ in the modelled interstellar cloud. Bottom: Ratios of abundances and column densities of $^{14}$N- and $^{15}$N-bearing species. Also indicated are the adopted elemental ratios of $^{14}$N/$^{15}$N and $^{14}$N$_2$/$^{14}$N$^{15}$N (dashed lines).

There is no indication in Fig. 7 for fractionation in the abundance of N$_2$ or N in the completely shielded interior of the interstellar cloud model ($A_V \gtrsim 3$). This is despite the inclusion of isotope-selective ion-molecule exchange reactions and a 40% faster rate of cosmic ray induced photodissociation for $^{14}$N$^{15}$N relative to $^{14}$N$_2$, given the physical parameters selected for this cloud model. Ultimately, cosmic-ray induced photodissociation is rendered irrelevant by faster and isotopologue-independent destruction mechanisms included in our model:

\[
{N}_2 \rightarrow N^+ + N \quad (12)
\]

and

\[
{N}_2 \rightarrow {N}_2H^+ \quad (13)
\]

The combined destruction rate due to these processes exceeds $10^{-13}$ s$^{-1}$ and is two orders of magnitude faster than cosmic-ray induced photodissociation.

The total-column fractionation of N and N$_2$ depends on the assumed depth of the modelled cloud, and is also plotted in Fig. 7 as a function of $A_V$. For our plane-parallel single-side-illuminated model this is maximal for $A_V$ between 1.5 and 2 mag, but never exceeds a factor of two for atomic or molecular species.

The minor contribution of cosmic-ray induced photodissociation to the nitrogen chemistry in our model does not presuppose a similar conclusion for other molecules, some of which have significantly higher cosmic-ray induced predissociation rates (Gredel et al., 1989).
5.2. Protoplanetary disc model

We have run a second chemical model for a vertical slice through a circumstellar disc using the same network of reactions as in Sec. 5.1. The model setup is identical to that of Visser et al. (2009) and Li et al. (2013). Briefly, we take the disc geometry, dust density and temperature distributions directly from the previous model of D'Alessio et al. (1999) without modification. This simulates a disc of mass $10^{-7}M_\odot$ and outer radius 400 AU surrounding a T Tauri star of mass 0.5 $M_\odot$ and radius 2 $R_\odot$. The simulated vertical slice is located at a radius of 105 AU.

A radiation field with the Draine wavelength dependence is perpendicularly incident on the surface of the slice, 120 AU above the midplane. The use of a scaled Draine field to represent the combined UV flux from the central star and the ISRF has been previously investigated in detail for the same disc geometry employed here (van Zadelhoff et al. 2003; Jonkheid et al. 2004). From these studies, a Draine field with $\chi = 516$ is a satisfactory proxy for a more realistic field including the details of the stellar spectrum at a disc radius of 105 AU. Dust grains of radius 1 $\mu$m are assumed to populate the disc which leads to weaker shielding and a greater penetration of ultraviolet radiation than for the interstellar cloud model of Sec. 5.1.

The abundances and cumulative column densities of atomic and molecular nitrogen in the disc model are plotted in Fig. 8. The abundance of $N_2$ becomes significant above 40 AU above the midplane and a rapid freeze-out of gaseous $N_2$ onto dust grains occurs 20 AU above the midplane, where the temperature falls below 20 K. The effect of photodissociative fractionation in the intervening 20 to 40 AU region is evident in the abundance ratios plotted in Fig. 9 where the atomic ratio of $^{14}N$/15N dips by a factor of 10 below the elemental ratio. However, fractionation of the total atomic N column is negligible because of its low abundance in this region. As for the interstellar cloud model, cosmic-ray induced photodissociation of $N_2$ is found to be negligible throughout the disc slice, and does not contribute to isotopic fractionation. Similarly, the contribution of ion-molecule exchange reactions to the calculated chemical abundances was found to be negligible following comparison with an alternative model where these are neglected. That is, the ice-phase predominance of nitrogen species in our model for disc heights with sufficiently low-temperature for chemical fractionation to occur suppresses these reactions.

The contribution of different species to the shielding of $^{14}N_2$ and $^{14}N^{15}N$ photodissociation were calculated as a function of height and $A_V$ and are plotted in Fig. 9. These calculations include all shielding species in an integral with the form in Eq. (5) by adopting column densities output from the disc model. From this, it is evident that shielding by 1 $\mu$m dust grains (approximated for Fig. 9 by assuming $\gamma_{dust} = 0.6$) and the hydrogen column are comparably effective. The shielding by CO is quite negligible because of the rarity of its overlaps with $N_2$, evident in Fig. 3. The significance of photodissociation-induced isotopic fractionation of atomic N relies on the relative importance of self-shielding of $^{14}N_2$ and $^{14}N^{15}N$. For $^{14}N_2$, this becomes important around 40 AU above the midplane and is comparable to dust and hydrogen shielding between 20 and 35 AU. For $^{14}N^{15}N$, self-shielding never contributes more than 10% of the total shielding and is about equivalent to its shielding by $^{14}N_2$.

The appearance of N and $N_2$ fractionation between 20 and 40 AU in Fig. 8 has consequences for other nitrogen bearing species. For example, Fig. 10 shows the abundances, column densities, and isotopic ratios of CN, HCN, and their ices; which are formed primarily from atomic N via the reactions

$$N + CH \rightarrow CN,$$

(14)

and

$$N + CH \rightarrow HCN.$$  

(15)

Additionally, CN and HCN are themselves susceptible to photodissociation and do not survive far from the midplane. Then, their maximum abundances occur within the region of enhanced $^{15}N$ atoms and this enhancement is mirrored in their integrated column densities. The isotopic fractionation of HCN gas and ices is plotted in Fig. 10 and approaches a factor of 10, whereas the fractionation of gaseous CN is somewhat less because a major portion of its column forms above 40 AU and outside the region of photo-fractionated N.

A different isotope fractionation pattern is evident in Fig. 11 for NH$_3$. The majority of the NH$_3$ population is frozen onto grain surfaces and its abundance has a sharp maximum at the inner edge of the $^{15}N/^{14}N$ fractionation zone, near 20 AU. We do not compute much difference between the integrated column densities of $^{14}NH_3$ and $^{15}NH_3$ in either gas or ice phases but the local $^{15}NH_3$ abundance is significantly enhanced and depleted in the ranges 20−25 and 25−40 AU, respectively. The pattern of NH$_3$ photolytic fractionation is more complex than for CN and HCN due to a more complex formation mechanism. There are two pathways leading to NH$_3$ in our model, the first occurring entirely in the gas phase and initiated from molecular N$_2$, that is,

$$N_2^{16}He \rightarrow N + N^* \rightarrow NH_3^+, \rightarrow NH_3,$$

(16)

and the second follows from the hydrogenation of atomic N after its condensation onto ice grains,

$$N \overset{T \leq 20 K}{\rightarrow} N ice \rightarrow NH_3 ice.$$  

(17)

Intermediate species NH and NH$_2$ in the reaction series summarised by Eq. (17) are also allowed to evaporate in our model and contribute to the gaseous NH$_3$ beginning with their ionisation by H$^+$, e.g.,

$$NH_2 + H^+ \rightarrow NH_3^+ \rightarrow NH_3.$$  

(18)

The balance between formation routes given in Eqs. (16), (17), and (18) dictates the height-dependent isotopic fractionation of NH$_3$ in sympathy with the fractionation of their respective precursors, N$_2$ or N. The occurrence of formation route (16) is limited to approximately 20 to 40 AU above the midplane, where there is an abundance of gaseous N$_2$. The process in Eq. (17) requires condensed atomic N and is even more restricted. That is, sufficiently low temperatures only occur within 25 AU of the midplane in our model, whereas the necessary source of gaseous N is limited to above 20 AU. Then, the NH$_3$ fractionation pattern resembles that of atomic N between 20 and 25 AU, and N$_2$ above this.

Overall, the complexity of photodissociative fractionation of NH$_3$ deduced here suggests the induced $^{14}NH_3$/$^{15}NH_3$ column density ratio in a particular environment will depend sensitively on its temperature and density profiles. The photodissociative fractionation of CN and HCN is likely more robust because the formation routes of these molecules are relatively simple. The enhancement of $^{15}N$ in CN and HCN within the self-shielding zone of our model disc (10x) is actually larger than for observations of cometary CN and HCN (2−3x) (Jebed et al. 2009).
This supports the feasibility of photodissociation as a mechanism for cometary fractionation. The greater fractionation of $^{15}\text{N}$ and HCN relative to $\text{NH}_2$ calculated for our particular protoplanetary disc also suggests that photodissociation may contribute to the explanation of a similar difference observed in the cold prestellar core L1544 (Hily-Blant et al. 2013), but not necessarily elsewhere in the galaxy (Daniel et al. 2013).

### 6. Conclusions

We used a high-resolution theoretical spectroscopic model of $^{14}\text{N}^{15}\text{N}$ to calculate its dissociation rate in interstellar space due to ultraviolet radiation, as well as the shielding of this radiation by dust grains and gas phase species. We obtain an unshielded rate of $1.73 \times 10^{-10}$ s$^{-1}$ assuming a Draine ISRF and an excitation temperature of 30 K, which is very near to the rate for $^{14}\text{N}_2$ obtained in our previous study (Li et al. 2013). Comprehensive tabulated shielding functions for $^{14}\text{N}_2$ and $^{14}\text{N}^{15}\text{N}$ are available online.\footnote{www.strw.leidenuniv.nl/~ewine/photo}

To calculate the rate of photodissociation in regions fully shielded from external radiation, the model of $^{14}\text{N}_2$ and $^{14}\text{N}^{15}\text{N}$ was combined with a detailed theoretical spectrum of H$_2$ emission arising from cosmic rays. Assuming $\zeta = 10^{-16}$ s$^{-1}$, a variable rate of $\sim 10^{-15}$ s$^{-1}$ was found to depend on the assumed details of the local environment, most significantly, the excitation temperature of $\text{N}_2$ and shielding species, the $o-\text{H}_2:p-\text{H}_2$ ratio, and the dust opacity at ultraviolet wavelengths. Isotope-dependent cosmic-ray induced photodissociation was also investigated, with the most extreme difference occurring when assuming 30 K, $o-\text{H}_2:p-\text{H}_2 = 0:1$, and a low dust absorption cross section appropriate to a protoplanetary disc experiencing grain growth. Then, the dissociation rate of $^{14}\text{N}^{15}\text{N}$ exceeds that of $^{14}\text{N}_2$ by a factor of 8. This large isotopic difference does not occur at a lower excitation temperature of 10 K. We also calculated the rate of CO dissociation by cosmic-ray induced photons previously determined by Gredel et al. (1987) using more accurate photodissociation cross sections, and deduced a $\sim$40% lower value.

Chemical models were run simulating an interstellar cloud and a protoplanetary disc to test the importance of self-shielding of external radiation and cosmic ray initiated photodissociation to the balance of $^{14}\text{N}$- and $^{15}\text{N}$-bearing species. An enhancement of atomic $^{15}\text{N}$ relative to $^{14}\text{N}$ is found at extinctions with $A_V \lesssim 3$, and is due to more effective self-shielding of the ISRF.
Fig. 9. Shielding functions for $^{14}\text{N}_2$ and $^{14}\text{N}^{15}\text{N}$ calculated for the protoplanetary disc model column densities. Partial shielding functions are shown considering dust grains only and with progressively more line absorption.

by $^{14}\text{N}_3$ than by $^{14}\text{N}^{15}\text{N}$. This fractionation is larger for our disc model where weaker dust shielding was assumed to simulate the growth and depletion of small dust grains. The photodissociation due to cosmic-ray induced ultraviolet radiation is found to be too slow to significantly influence the chemistry in the dark interiors of our models.

The isotopically-dependent photodissociation of $\text{N}_2$ in our protoplanetary disc model leads to a significant enhancement in the column densities of HC$^{15}\text{N}$ relative to HC$^{14}\text{N}$. Our model predicts a value of HC$^{14}\text{N}$/HC$^{15}\text{N} \approx 100$, when assuming an elemental nitrogen abundance ratio of $^{14}\text{N}/^{15}\text{N} = 450$. This corresponds to an isotopic fractionation in $\delta$-notation of $^{15}\text{N}\text{HCN} \approx -800\%$. This enhancement mirrors the fractionation of atomic $\text{N}$ induced by photodissociation. Our model predicts a lower fractionation ratio for CN, with C$^{13}\text{N}$/C$^{12}\text{N} \approx 250$. This is because the region where CN forms does not coincide as neatly with the peak of $\text{N}_2$ isotopic dependent photodissociation. The formation chemistry of $\text{NH}_3$ is more complex and can be initiated from both $\text{N}_2$ and atomic $\text{N}$. This species is then less fractionated in our model.

Many assumptions must be made when modelling the chemistry of complex and remote objects such as protoplanetary discs. However, the calculations underpinning our predictions of photodissociative fractionation are based on reliable laboratory and theoretical spectroscopy and may be resilient to many structural details of astrophysical objects.

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