Measurement of $CP$-Violating Asymmetry $\sin 2\beta$ with the BABAR Detector

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1 Introduction

The Standard Model of electroweak interactions describes $CP$ violation in weak interactions as a consequence of a complex phase in the three-generation Cabibbo-Kobayashi-Maskawa (CKM) quark-mixing matrix \[ |V_{ud}|^2 + |V_{ub}|^2 + |V_{cd}|^2 + |V_{cb}|^2 + |V_{td}|^2 + |V_{tb}|^2 \]. In this framework, measurements of $CP$-violating asymmetries in the time distribution of neutral $B$ decays to charmonium final states provide a direct measurement of $\sin 2\beta$ \[^2\], where $\beta \equiv \arg \left[ -V_{cd}V_{cb}^*/V_{td}V_{tb}^* \right]$.

We report an updated measurement of time-dependent $CP$-asymmetries in samples of fully reconstructed $B$ decays to charmonium-containing $CP$ eigenstates ($b \to c\bar{s}s$). The data for these studies were recorded at the $\Upsilon(4S)$ resonance with the BABAR detector at the PEP-II asymmetric-energy $e^+e^-$ collider at the Stanford Linear Accelerator Center.

We fully reconstruct a sample of neutral $B$ mesons, $B_{CP}$, decaying to several $CP$ final states. Each event in the $B_{CP}$ is examined for evidence that the recoiling neutral $B$ meson decayed as a $B^0$ or $\bar{B}^0$ (flavor tag). The time distribution of $B$ meson decays to a $CP$ eigenstate with a $B^0$ or $\bar{B}^0$ tag can be expressed in terms of a complex parameter $\lambda$ that depends on both the $B^0-\bar{B}^0$ oscillation amplitude and the amplitudes describing $\bar{B}^0$ and $B^0$ decays to this final state \[^3\]. The decay rate $f_+(f_-)$ when the tagging meson is a $B^0(\bar{B}^0)$ is given by
\[ f_{\pm}(\Delta t) = \frac{e^{-|\Delta t|/\tau_{B^0}}}{4\tau_{B^0}} \times \left[ 1 \pm \frac{2Tm\lambda}{1+|\lambda|^2} \sin(\Delta m_d \Delta t) \mp \frac{1-|\lambda|^2}{1+|\lambda|^2} \cos(\Delta m_d \Delta t) \right], \quad (1) \]

where \( \Delta t = t_{\text{rec}} - t_{\text{tag}} \) is the difference between the proper decay times of the reconstructed \( B \) meson (\( B_{\text{rec}} \)) and the tagging \( B \) meson (\( B_{\text{tag}} \)), \( \tau_{B^0} \) is the \( B^0 \) lifetime, and \( \Delta m_d \) is the \( B^0 - \overline{B^0} \) oscillation frequency.

In the Standard Model \( \lambda = \eta_f e^{-2i\beta} \) for charmonium-containing \( b \to c\bar{c}s \) decays and \( \eta_f \) is the \( CP \) eigenvalue of the state \( f \). Thus, the time-dependent \( CP \)-violating asymmetry is

\[ A_{CP}(\Delta t) \equiv \frac{f_{+}(\Delta t) - f_{-}(\Delta t)}{f_{+}(\Delta t) + f_{-}(\Delta t)} = -\eta_f \sin 2\beta \sin (\Delta m_{B^0} \Delta t), \quad (2) \]

with \( \eta_f = -1 \) for \( J/\psi K^0_S, \psi(2S)K^0_S \), and \( \chi_{c1}K^0_S \), and +1 for \( J/\psi K^0_L \).

The measurement of \( \sin 2\beta \) with the decay mode \( B \to J/\psi K^{*0}(K^{*0} \to K^0_S\pi^0) \) is experimentally complicated by the presence of both even (\( L=0,2 \)) and odd (\( L=1 \)) orbital angular momenta in the final state. The decay rate \( f_{+}(\Delta t) \) when the tagging meson is a \( B^0(\overline{B^0}) \), in addition to \( \Delta t \), is also a function of the angular distribution of the particles in the final state.

## 2 The \textit{BABAR} detector

A detailed description of the \textit{BABAR} detector can be found in Ref. [2]. Charged particles are detected and their momenta measured by a combination of a silicon vertex tracker (SVT) consisting of five double-sided layers and a central drift chamber (DCH), in a 1.5-T solenoidal field. The average vertex resolution in the \( z \) direction is 70 \( \mu \)m for a fully reconstructed \( B \) meson. We identify leptons and hadrons with measurements from all detector systems, including the energy loss (\( dE/dx \)) in the DCH and SVT. Electrons and photons are identified by a CsI electromagnetic calorimeter (EMC). Muons are identified in the instrumented flux return (IFR). A Cherenkov ring imaging detector (DIRC) covering the central region, together with the \( dE/dx \) information, provides \( K-\pi \) separation of at least three standard deviations for \( B \) decay products with momentum greater than 250 MeV/c in the laboratory.

## 3 Data Sample

The data sample used in this analysis consists of approximately 56 fb\(^{-1} \), corresponding to about 62 million \( B\overline{B} \) pairs, collected on the \( \Upsilon(4S) \) resonance with the \textit{BABAR} detector at the SLAC PEP-II storage ring between October 1999 and December 2001.
We fully reconstruct $B$ candidates in the final states $J/\psi K^0_S (K^0_S \rightarrow \pi^+\pi^-)$, $J/\psi K^0_S (K^0_S \rightarrow \pi^0\pi^0)$, $\psi(2S)K^0_S$, and $\chi_{c1} K^0_S$, $J/\psi K^{*0}(K^{*0} \rightarrow K^0_S\pi^0)$, and $J/\psi K^0_L$ as described in Ref. [4]. Figure 2 shows the distribution of the beam-energy substituted mass $m_{ES}$ for this sample.

4 The Measurement Technique

A measurement of $A_{CP}$ requires a determination of the experimental $\Delta t$ resolution and the fraction $w$ of events in which the tag assignment is incorrect. This mistag fraction reduces the observed $CP$ asymmetry by a factor $(1 - 2w)$. Mistag fractions and $\Delta t$ resolution functions are determined from a large sample $B_{flav}$ of neutral $B$ decays to flavor eigenstates consisting of the channels $D^{(*)-}h^+(h^+ = \pi^+, \rho^+, \text{and } a_1^+)$ and $J/\psi K^{*0}(K^{*0} \rightarrow K^+\pi^-)$. Figure 3 shows the distribution of the beam-energy substituted mass $m_{ES}$ for this sample.
Figure 2: Beam-energy substituted mass distribution for the $B_{\text{flav}}$ sample. In 56 fb$^{-1}$, we reconstruct about 17500 signal events. Average signal purity for $m_{ES} > 5.27$ GeV/c$^2$ is 85 %.

4.1 $B$ Flavor-Tagging Algorithm

The algorithm used to determine the flavor of the tagging $B$ meson $B_{\text{tag}}$ is described in Ref. [6]. The charges of energetic electrons and muons from semileptonic $B$ decays, kaons, soft pions from $D^*$ decays, and high momentum particles are correlated with the flavor of the decaying $b$ quark. For example, a positive lepton indicates a $B_0^*$ tag.

Each event is assigned to one of four hierarchical, mutually exclusive tagging categories or has no flavor tag. A lepton tag requires an electron (muon) candidate with a center-of-mass momentum $p_{\text{cm}} > 1.0$ (1.1) GeV/c. This efficiently selects primary leptons and reduces contamination due to oppositely-charged leptons from charm decays. Events meeting these criteria are assigned to the Lepton category unless the lepton charge and the net charge of all kaon candidates indicate opposite tags. Events without a lepton tag but with a non-zero net kaon charge are assigned to the Kaon category. All remaining events are passed to a neural network algorithm whose main inputs are the momentum and charge of the track with the highest center-of-mass momentum, and the outputs of secondary networks, trained with Monte Carlo samples to identify primary leptons, kaons, and soft pions. Based on the output of the neural network algorithm, events are tagged as $B^0$ or $\bar{B}^0$ and assigned to the NT1 (more certain tags) or NT2 (less certain tags) category, or not tagged at all. The tagging power of the NT1 and NT2 categories arises primarily from soft pions and from recovering unidentified isolated primary electrons and muons.

The tagging efficiencies $\varepsilon_i$ and mistag fractions $w_i$ for the four tagging categories are measured from data and summarized in Table [1].
Figure 3: Topology of an event where one $B$ meson is fully reconstructed in a $CP$ eigenstate and the flavor of the other $B$ meson is determined from its decay products.

4.2 $\Delta t$ Measurement and Resolution Function

The topology of a typical $CP$ event is shown in Figure 3. The time interval $\Delta t$ between the two $B$ decays is calculated from the measured separation $\Delta z$ between the decay vertices of $B_{\text{rec}}$ and $B_{\text{tag}}$ along the collision ($z$) axis [6]. We determine the $z$ position of the $B_{\text{rec}}$ vertex from its charged tracks. The $B_{\text{tag}}$ decay vertex is determined by fitting tracks not belonging to the $B_{\text{rec}}$ candidate to a common vertex, employing constraints from the beam spot location and the $B_{\text{rec}}$ momentum [6]. We accept events with a $\Delta t$ uncertainty of less than 2.5 ps and $|\Delta t| < 20$ ps. The fraction of events satisfying these requirements is 93%. The r.m.s. $\Delta t$ resolution for 99.5% of

| Category | Efficiency (%) | $w$       | $\Delta w$   |
|----------|---------------|-----------|--------------|
| Lepton   | 11.1 ± 0.2    | 8.6 ± 0.9 | 0.6 ± 0.5    |
| Kaon     | 34.7 ± 0.4    | 18.1 ± 0.7| −0.9 ± 0.1   |
| NT1      | 7.7 ± 0.2     | 22.0 ± 1.5| 1.4 ± 0.3    |
| NT2      | 14.0 ± 0.3    | 37.3 ± 1.3| −4.7 ± 0.9   |
| All      | 67.5 ± 0.5    |           |              |
these events is 1.1 ps.

The $\Delta t$ resolution function for the signal is represented in terms of $\delta_t \equiv \Delta t - \Delta t_{\text{true}}$ by a sum of three Gaussian distributions with different means and widths:

$$R(\delta_t) = \sum_{k=\text{core, tail}} \frac{f_k}{S_k \sigma_{\Delta t} \sqrt{2\pi}} \exp \left( -\frac{(\delta_t - b_k \sigma_{\Delta t})^2}{2(S_k \sigma_{\Delta t})^2} \right) + \frac{f_{\text{outlier}}}{\sigma_{\text{outlier}} \sqrt{2\pi}} \exp \left( -\frac{\delta_t^2}{2\sigma_{\text{outlier}}^2} \right).$$

For the core and tail Gaussians, we use two separate scale factors $S_k$ to multiply the measured uncertainty $\sigma_{\Delta t}$ that is derived from the vertex fit for each event. The scale factor for the tail component is fixed to the value found in simulated data since it is strongly correlated with the other resolution function parameters. The core and tail Gaussian distributions are allowed to have non-zero means to account for any daughters of long-lived charm particles included in the $B_{\text{tag}}$ vertex. The mean of the core Gaussian is allowed to be different for each tagging category, but only one common mean is used for the tail component. These offsets are computed from the event-by-event $\sigma_{\Delta t}$ multiplied by a scale factor $b_k$ which accounts for a correlation between the mean of the $\delta_t$ distribution and $\sigma_{\Delta t}$ observed in simulated events. The outlier Gaussian has a fixed width of 8 ps and no offset; it accounts for less than 0.5% of events with incorrectly reconstructed vertices. In simulated events we find no significant difference between the $\Delta t$ resolution function of the $B_{\text{CP}}$ and the $B_{\text{flav}}$ samples, hence the same resolution function is used for both.

## 5 Results

We determine $\sin^2 \beta$ with a simultaneous unbinned maximum likelihood fit to the $\Delta t$ distributions of the tagged $B_{\text{CP}}$ and $B_{\text{flav}}$ samples. In this fit the $\Delta t$ distributions of the $B_{\text{CP}}$ sample are described by Eq. [1] with $|\lambda| = 1$. The $\Delta t$ distributions of the $B_{\text{flav}}$ sample evolve according to the known frequency for flavor oscillation in $B^0$ mesons. The observed amplitudes for the $CP$ asymmetry in the $B_{\text{CP}}$ sample and for flavor oscillation in the $B_{\text{flav}}$ sample are reduced by the same factor $1 - 2w$ due to flavor mistags. Events are assigned signal and background probabilities based on the $m_{ES}$ (all modes except $J/\psi K^{*0}$ and $J/\psi K^{0}_L$) or $\Delta E$ ($J/\psi K^{0}_L$) distributions. The $\Delta t$ distributions for the signal are convolved with the resolution function described in Section 4.2. Backgrounds are incorporated with an empirical description of their $\Delta t$ spectrum, containing prompt and non-prompt components convolved with a resolution function [F] distinct from that of the signal.

There are 35 free parameters in the fit: $\sin^2 \beta$ (1), the average mistag fractions $w$ and the differences $\Delta w$ between $B^0$ and $\bar{B}^0$ mistag fractions for each tagging category (8), parameters for the signal $\Delta t$ resolution (8), and parameters for background time dependence (6), $\Delta t$ resolution (3), and mistag fractions (8). In addition, we allow $\cos^2 \beta$ (1), which is determined from the $J/\psi K^{*0}$ events, to vary in the fit [4]. We
fix $\tau_{B^0}$ and $\Delta m_d$ [7]. The determination of the mistag fractions and $\Delta t$ resolution function parameters for the signal is dominated by the high-statistics $B_{\text{flav}}$ sample. The largest correlation between $\sin^2 \beta$ and any linear combination of the other free parameters is 0.14.

Figure 4 shows the $\Delta t$ distributions and $A_{\text{CP}}$ as a function of $\Delta t$ overlaid with the likelihood fit result for the $\eta_f = -1$ and $\eta_f = +1$ samples. The fit to the $B_{\text{CP}}$ and $B_{\text{flav}}$ samples yields

$$\sin^2 \beta = 0.75 \pm 0.09 \text{ (stat)} \pm 0.04 \text{ (syst)}.$$  

The dominant sources of systematic error are the uncertainties in the level, composition, and $CP$ asymmetry of the background in the selected $CP$ events (0.022), limited Monte Carlo simulation statistics (0.014), and the assumed parameterization of the $\Delta t$ resolution function (0.013), due in part to residual uncertainties in the internal alignment of the vertex detector. Uncertainties in $\Delta m_d$ and $\tau_{B^0}$ each contribute 0.010 to the systematic error. The large sample of reconstructed events allows a number of consistency checks, including separation of the data by decay mode, tagging category and $B_{\text{tag}}$ flavor. The results of fits to some subsamples and to the samples of non-$CP$ decay modes are shown in Table 2. For the latter, no statistically significant asymmetry is found.

With the theoretically preferred choice of the strong phases, consistent with the hypothesis of the $s$-quark helicity conservation in the decay [8], the parameter $\cos^2 \beta$ is measured to be $+3.3^{+0.6}_{-1.0} \text{ (stat)}^{+0.6}_{-0.7} \text{ (syst)}$ [4].

If the parameter $|\lambda|$ in Eq. 1 is allowed to float in the fit to the $\eta_f = -1$ sample, which has high purity and requires minimal assumptions on the effect of backgrounds, the value obtained is $|\lambda| = 0.92 \pm 0.06 \text{ (stat)} \pm 0.02 \text{ (syst)}$. The sources of the systematic error are the same as for the $\sin^2 \beta$ measurement with an additional contribution in quadrature of 0.012 from the uncertainty on the difference in the tagging efficiencies for $B^0$ and $\bar{B}^0$ tagged events. In this fit, the coefficient of the $\sin(\Delta m_d \Delta t)$ term in Eq. 1 is measured to be $0.76 \pm 0.10 \text{ (stat)}$ in agreement with Table 2.

### Table 2: Number of tagged events, signal purity and observed $CP$ asymmetries in the $CP$ samples and control samples. Errors are statistical only.

| Sample | $N_{tag}$ | Purity (%) | $\sin^2 \beta$ |
|--------|-----------|------------|----------------|
| $J/\psi K^0_S,\psi(2S)K^0_S,\chi_{c1} K^0_S$ | 995 | 94 | 0.76 ± 0.10 |
| $J/\psi K^0_L$ | 742 | 57 | 0.73 ± 0.19 |
| $J/\psi K^{*0}, K^{*0} \rightarrow K^0_S \pi^0$ | 113 | 83 | 0.62 ± 0.56 |
| **Full $CP$ sample** | 1850 | 79 | 0.75 ± 0.09 |
| $B_{\text{flav}}$ non-$CP$ sample | 17546 | 85 | 0.00 ± 0.03 |
| Charged $B$ non-$CP$ sample | 14768 | 89 | -0.02 ± 0.03 |
6 Summary

We have presented a new preliminary measurement of CP-violating asymmetry \( \sin 2\beta \) using a sample of fully reconstructed \( B \) mesons decaying into CP final states.

Ever since this Conference we have further improved the analysis and updated our measurement [10]. Changes in the analysis with respect to the result presented here include a new flavor-tagging algorithm and the addition of the decay mode \( B^0 \to \eta_c K^0_s \). The new result \( \sin 2\beta = 0.741 \pm 0.067 \text{ (stat)} \pm 0.033 \text{ (syst)} \) improves upon and supersedes the result presented at this Conference and provides the most precise measurement of \( \sin 2\beta \) currently available. It is consistent with the range implied by measurements and theoretical estimates of the magnitudes of CKM matrix elements in the context of the Standard Model [11].
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