ON THE SEARCH FOR TRANSITS OF THE PLANETS ORBITING GL 876

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ABSTRACT

We report the results of a globally coordinated photometric campaign to search for transits by the Gl 876 planetary system. These two planets experience strong mutual perturbations, which necessitate use of a dynamical (four-body) model to compute transit ephemerides for the system. Our photometric data have been collected from published archival sources, as well as from our photometric campaigns that were targeted to specific transit predictions. Our analysis indicates that transits by planet “c” (P ∼ 30 d) do not currently occur, in concordance with the best-fit i = 50° co-planar configuration obtained by dynamical fits to the most recent radial velocity data for the system. Transits by planet “b” (P ∼ 60 d) are not entirely ruled out by our observations, but our data indicate that it is very unlikely that they occur. Our experience with the Gl 876 system suggests that a distributed ground-based network of small telescopes can be used to search for transits of very low mass M-stars by terrestrial-sized planets.

Subject headings: stars: planetary systems – stars: individual (Gl 876) – planets and satellites: general

1. INTRODUCTION

The Gl 876 planetary system ranks with the most remarkable discoveries that have emerged from the first decade of extrasolar planet detections. As described by Butler et al. (2001), Marcy et al. (2001), Delfosse et al. (1998) and Marcy et al. (1998), there are a number of reasons why the Gl 876 planets are extraordinary. Planet “d”, with its 1.974 day orbit and M sin(i) = 5.9M⊕ is the lowest-mass exoplanet known to orbit a nearby main-sequence star (Rivera et al. 2005). Planets “c” and “b” are the only Jovian-mass companions known to orbit an M-dwarf, and their clear participation in 2:1 mean-motion resonance gives important dynamical clues to the formation and evolution of the system (e.g. Lee and Peale 2002). Furthermore, the Gl 876 planets are the closest exoplanets that have been reliably characterized. Their radial velocity amplitudes induce an overall signal-to-noise of nearly 100, and they have been observed for well over a decade.

The detection of Gl 876 d by Rivera et al. (2005) underscored the rapid development of the Doppler technique. The detection of planets having only a few Earth masses is the culmination of advances described by Butler et al. (1996), Marcy & Butler (1998), Marcy, Cochran, & Mayor (2000), Marcy et al. (2005), and Lovis et al. (2006). Nevertheless, while radial velocity precision has improved to better than 1 m/s, Keplerian orbital fits to Doppler velocities give estimates of M pl sin(i) rather than M pl. In order to ascertain the true mass of a planet, one must obtain an independent measure of the orbital inclination, i, which is most easily measured when the planet is observed to transit across the face of the parent star.

The now-celebrated companion to HD 209458 provided the first example of a transiting extrasolar planet, and this body has generated an incredible variety of observational and theoretical investigations. HD 209458b was initially detected with the radial velocity method, and was then discovered to transit on the basis of follow-up photometric observations at the predicted transit times (Henry et al. 1999, 2000; Charbonneau et al. 2000). HD 209458b’s well-sampled light curve, when combined with high-precision radial velocity data, has permitted precise measurements of the planet’s basic attributes (e.g. Mazeh et al. 2000, Brown et al. 2001, Laughlin et al. 2005, Winn & Holman 2005).

To date, nine additional planets have been found to transit their parent stars, and the varied uses to which these transits have been put are described in the review article by Charbonneau et al. (2006). Our goal in this paper is to ascertain whether the two outer planets orbiting Gl 876 (IL Aqr, GJ 876, HIP 113020) can similarly be observed in transit. A positive detection would give a further major improvement in our understanding both of this specific system and of planetary properties in general.

Rivera et al. (2005) carried out a photometric search
for transits by planet d ($P \sim 1.974$ d), and showed that such transits do not occur. To date, photometric searches for transits by planet c ($P \sim 30$ d) and b ($P \sim 60$ d) have not been reported. Although the a priori geometric transit probabilities for Gl 876 c and b are only $P_{tr} = 1.4\%$ and $P_{tr} = 0.9\%$, respectively, the expected photometric transit depths are greater than 10\%. Librational motions arising from the resonance between the two outer planets lead to predicted transit epochs for the outer planets that are not spaced evenly in time. (The resonant structure of the system is discussed further in Laughlin & Chambers 2001; Rivera & Lissauer 2001; Kley 2003; and Beaugé, Michtchenko, & Ferraz-Mello 2005.)

Benedict et al. (2002) used HST astrometry to derive an orbital inclination for Gl 876b of $i = 84 \pm 6\%$. Their result thus suggests that planet b has a mass equal or close to the RV-determined value of $M \sin(i) = 1.89 M_{\text{Jup}}$, and that the system is within 1-sigma of being viewed edge-on. The implication of the Benedict et al. (2002) measurement is that occurrence of transits is much more likely than the a-priori geometric probability would suggest. The Benedict et al. (2002) result is in conflict, however, with the dynamical models of the system presented by Rivera et al. (2005), who find a best fit to the radial velocity data when the system (assumed co-planar) is inclined by $i \sim 50 \pm 3\%$ with respect to the plane of the sky. Therefore, if transits are detected, then the Benedict et al. (2002) results will be confirmed at the expense of the conclusions of Rivera et al. (2005).

Gl 876b and Gl 876c are members of an as-yet unobserved class of giant planets with intermediate surface temperatures. The expected effective temperatures of $T_{\text{eff,b}} = 160$ K and $T_{\text{eff,c}} = 200$ K of the planets are much lower than the value $T_{\text{eff}} \sim 1350$ K measured with Spitzer for HD 209458b (Charbonneau et al. 2005), but still considerably higher than the $T_{\text{eff}} \sim 135$ K measured for Jupiter. Determination of their physical properties would thus provide a useful link between Jupiter and Saturn on the one hand, and objects such as HD 209458b on the other. Accurate measurement of their radii would also give clues to their interior structure (see Charbonneau et al. 2006).

Finally, the Gl 876 system with its strongly gravitationally interacting planets and large planet-to-star radius ratios, has the potential to display an extraordinarily informative set of transit light curves. Our model light curves herein show what one can expect when interacting transiting systems are discovered, for example, with ongoing radial velocity surveys or with space-based missions such as Kepler (Borucki et al. 2003) or COROT (Baglin 2003), and allow for a more complete understanding of the multiplanet dynamics.

The plan of this paper is as follows. In §2, we describe our dynamical model of the system, and illustrate some of the photometric properties that the in-transit light-curves would be expected to display. In §3, we describe an evaluation of the Doppler radial velocity measurements that have been taken during predicted transit intervals. In §4, we evaluate a range of archival and newly obtained photometric data sets for evidence of transits. In §5, we discuss our results, as well as the current status and outlook for the ongoing TransitSearch collaboration, and in §6, conclude.
appropriate to V-band observations of an M4V primary (per Claret 2000); and $\mu = \cos(\theta)$.

Figures 2 and 3 show a selection of model light curves for planets b and c. For planet b, which has an eccentricity ($e = 0.22$), rapidly precessing orbit ($d\varpi/dt \sim 44^\circ$ yr$^{-1}$), the shape of the predicted curves depends strongly on the osculating periastron angle. For $i < 90^\circ$, the transits are both shorter and deeper when the transits occur near periastron. The orbital eccentricity of planet b is more nearly circular, with $e = 0.025$. In this case, there is little variation in the predicted light curves as the orbits precess. The known transiting planets have transit-to-transit intervals $\Delta T_i$ that are evenly spaced to within the current resolution of the observations. HD 209458b, for example, has had individual transit midpoints measured to an accuracy of several seconds (Brown et al. 2001, Wittenmyer et al. 2005), and an average period measured to an accuracy of 83 ms (Wittenmyer et al. 2005, Winn & Holman 2005). If, however, one is able to measure differences in the time intervals between successive transits, one can derive additional dynamical information. As discussed by Miralda-Escudé (2002), Holman & Murray (2005), and Agol et al. (2005), measurements of small variations from exact periodicity can be used to infer the presence of additional bodies in the system, potentially with the masses in the range appropriate to terrestrial planets. In the event that either Gl 876b or Gl 876c were to transit, one would expect the departures from strict periodicity to be large. In fact, successive transits of planet c would occur at intervals differing by as much as 4 hours! By fitting a dynamical model to such transit intervals, one could obtain information regarding all of the orbital elements of the planets (including inclinations and nodes).

3. SEEKING EVIDENCE OF TRANSITS IN THE RADIAL VELOCITY DATA SET

During a planetary transit, the occulting disk of the planet passes over portions of the stellar disk containing a varying component of line-of-sight velocity arising from stellar rotation; this phenomena produces an asymmetry in the star’s spectral lines known as the Rossiter-McLaughlin effect (Rossiter 1924, McLaughlin 1924). The effect has been described in detail in the context of planetary transits by Ohta, Taruya & Suto (2005), and has been analyzed for HD 209458 by Queloz et al. (2000), Bundy & Marcy (2000), and Winn et al. (2005), and for HD 149026 by Wolf et al. (2006). In fact, the transiting planet HD 189733 was initially discovered to transit not via photometry, but rather via such in-transit radial velocity variations, found by Bouchy et al. (2005). For our study of Gl 876, we compared the observation epochs of all of the Lick (see Marcy et al. 2001) and Keck (see Rivera et al. 2005) radial velocity observations to see if any of these observations occurred during a predicted transit (assuming $i = 90^\circ$). For Gl 876, we used a rotational period that was determined to be 96.7 days using rotational modulation (as reported in Rivera et al. 2005); we used this value to calculate the amplitude of the Rossiter-McLaughlin effect. Four such observations were found, three taken during a predicted transit by planet “c”, and one taken during a predicted transit by planet “b”. Figures 4 and 5 display the relevant parts of the radial velocity model (both with and without the Rossiter-McLaughlin effect), with the observations shown. The radial velocity model curves in both figures were generated by adding template curves which use the stellar and planetary radii and limb darkening law given above (and which apply the analytic integrals given in Ohta et al. 2005), to our fiducial $i = 90^\circ$ three-planet radial velocity model. For the transit epoch in the case of planet c (Figure 4), the data is inconsistent with a transit. In Figure 5, for the outer planet b, the situation is unresolved.

4. A SEARCH FOR TRANSITS IN PHOTOMETRIC DATA SETS

We have also compared our model light curves to a variety of photometric datasets for Gl 876 taken since 1989. The results of these comparisons are as follows.

Hipparccos: The Hipparcos Mission (see Perryman et al. 1997) produced 67 accepted photometric measurements for Gl 876 (HIP 115302). These measurements have a median magnitude $H_p = 10.148$, with $\sigma = 0.0045$. There is evidence for a weak periodicity when the data is folded at the 96.7 d rotational period of the star (also noted in Rivera et al. 2005). In Figure 6, we plot our model $i = 89.6^\circ$ light curves for Gl 876 b and c superimposed on the Hipparcos epoch photometry. None of the Hipparcos measurements were made near or during a predicted transit window.

Fairborn Observatory: A number of long-term photometric monitoring programs are being carried out with the automated telescopes at Fairborn Observatory (e.g., Henry 1999; Eaton, Henry, & Fekel 2003) and, as described in detail in Rivera et al. (2005), Gl 876 has been on one of the observing programs. Figures 7 and 8 show the Fairborn Observatory data and our corresponding model light curve for planets b and c. Data taken during predicted transit epochs for planet c show no indication of a transit. The Fairborn Observatory data indicate that long-term stellar variability from Gl 876 is of order 0.05 magnitude, which is somewhat smaller than the variation observed with Hipparcos.

TransitSearch and AAVSO: Seagroves et al. (2003) describe TransitSearch, a cooperative distributed observing project involving sub-meter class telescopes worldwide. The TransitSearch strategy is to observe known planet-bearing stars at the dates and times when transits are expected to occur. It is therefore a targeted search, which differentiates it from ongoing wide-field surveys. We identify observing windows for candidate stars through the use of the bootstrap Monte Carlo technique described by Laughlin et al. (2005). The observational campaigns are prioritized by the a-priori likelihood that a particular candidate planet will display transits. This likelihood is given by,

$$P_{\text{transit}} = 0.0045 \left( \frac{1 \text{AU}}{a} \right) \left( \frac{R_\star + R_{\text{pl}}}{R_\odot} \right) \left[ \frac{1 + e \cos(\frac{\varpi}{2} - \varphi)}{1 - e^2} \right]$$

where $a$ is the semi-major axis of the orbit, $R_\star$ is the radius of the star, $R_{\text{pl}}$ is the radius of the planet, $\varpi$ is the longitude of periastron, and $e$ is the orbital eccentricity.

The first TransitSearch dataset for Gl 876 was obtained by one of us (Shankland) from 2003 Oct. 27.9583 to 2003 Oct. 28.0368, with a V-filtered, 16-bit speckle ccd at the
primary focus of a 40.4 cm f/5.1 reflector (at air mass from sec(z) = 2.7 to 1.7). The photometric time series shows a monotonic flux increase of 0.16 +/- 0.04 mag from 2003 Oct. 27.9583 to 2003, Oct 27.9972. As shown on the left panel of Figure 9, the depth, duration and timing of this event were consistent with an egress from transit of Gl 876 c, in agreement with our predictions. The possibility that a transit had been observed spurred us to orchestrate a distributed observational campaign during the 2004 season.

During the 2004 June 24 opportunity, observations were attempted by ten observers in Australia. Poor weather thwarted all but one observer, and no transit signal was seen in the data, which covered about half of the 1 – σ transit window. Eight Australian and Japanese observers participated in the following 2004 July 24 planet c campaign. They were all clouded out. Weather improved for the 2004 August 23 planet c opportunity, permitting observations by five of the nine Australian, South African, and German observers. No transit signal was seen with photometric depth greater than 1%.

In 2004 October, a number of AAVSO and TransitSearch observers obtained photometry during a closely spaced pair of transit windows for planets b and c. Beginning October 20 11:22 UT and ending October 23 15:27 UT, a total of 2,795 CCD observations were obtained. In addition, 2,981 photometric observations were obtained in the days immediately before and after the window to set baseline activity and to look for red dwarf flaring. Such a large, distributed network of observers allowed coverage of the window with very few observing gaps over the 3-day period. Gaps in the coverage were smaller than the estimated transit period or forecast window, allowing us to conclude that transits for planets b and c did not occur during the October 2004 campaign. Photometric data from the campaign are plotted in Figures 9 and 10.

Individual observations and uncertainty estimates from the October 2004 campaign are available from the AAVSO web site, while the other datasets can be found at the TransitSearch website14. We are continuing to obtain photometry of Gl 876, with the goal of gaining a better understanding of the photometric variability of mature (age exceeding 1Gyr) red dwarfs.

5. DISCUSSION

The TransitSearch photometric network has been in operation for three years, and has participating observers capable of providing fully global longitude and latitude coverage. The network maintains a continuously updated catalog15 of the known census of extrasolar planets. The catalog is presently the only available source for (1) a-priori transit probabilities and predicted transit depths, for the known extrasolar planets, (2) predicted transit ephemerides and transit window uncertainties based on orbital fits to published radial velocities, and (3) the results of known photometric searches for transits of planet-bearing stars. To date, the majority of negative transit searches have not been reported in the literature. With this paper, we hope to spur a reversal of that trend.

Due to significant uncertainties in the orbital fits, it is generally very difficult to definitively rule out transits by planets with P > 10d. The Gl 876 planets form a notable exception to this rule because of their high signal-to-noise, Γ ~ 50, and the extensive radial velocity data set allows for a very accurate orbital fit. Campaigns by the TransitSearch collaboration have thus far led to transits of a number of other shorter-period planet-bearing stars being ruled out to a high degree of confidence. The planets for which the possibility of transits have been significantly discounted by our campaigns include HD 217107 “b” (P = 7.127d, P95 = 8.0%, see also Vogt et al. 2005), HD 168746 “b” (P = 6.403d, P95 = 8.1%, see also Pepe et al. 2002), and HD 68988 “b” (P = 6.276d, P95 = 9.0%, see also Vogt et al. 2002).

Furthermore, planets for which usable photometry of the parent stars has been obtained by our network during the 3 – σ transit windows, but for which transits can not yet be fully ruled out, include HD 188753 Ab (P = 3.348d, P95 = 11.8%), HD 76700 “b” (P = 3.971d, P95 = 10.0%), HD 13445 b (P = 15.76d, P95 = 3.4%), HD 74156 “b” (P = 51.64d, P95 = 3.8%), HD 37605 “b” (P = 54.23d, P95 = 2.2%), and HD 80606 “b” (P = 111.4d, P95 = 1.7%). Planets for which campaigns are scheduled to begin soon include GL 581 “b” (P = 5.366d, P95 = 3.6%), and HD 99492 “b” (P = 17.04d, P95 = 3.4%). GL 581 is of particular interest because the primary star is an M dwarf, and the planet (if it transits) will be a Neptune-mass object M sin(i) = 0.052MJup (Bonfils et al. 2005). The 1.6% transit depth would allow an unprecedented physical characterization of a low-mass extrasolar planet. To date, our Gl 876 campaign has employed the most globally far-reaching distribution, and along with recent leaps in fidelity in similar campaigns, clearly underscores the utility of the network.

What is more, Gl 876 b and c constitute a dramatic exception to the emerging aphorism that Jupiter-mass planets are rarely associated with M dwarfs. Indeed, a paucity of giant planets orbiting red dwarfs seems to be a natural consequence of the core accretion theory of planet formation (Laughlin, Bodenheimer & Adams 2004). The core-accretion theory predicts, however, that Neptune-mass and smaller mass planets will be very common around red dwarfs. This stands in contrast to the predictions of Boss (2006), who suggests that the gravitational instability mechanism is the dominant mode of giant planet formation. If this is true, then Jupiter-mass planets should be as common around red dwarfs as they are around solar-type stars. Efforts to detect transits of small planets orbiting small stars are therefore likely to gain increasing importance and focus over the next several years.

There are, in fact, several observational indications that low-mass planets may be common around red dwarfs. The radial velocity surveys have recently reported the detection of Neptune-mass companions in short-period orbits around the red dwarfs GL 581 and GL 436. The OGLE team of observers using the microlensing method have detected the signature of what appears to be a planet with 5.5 Earth Masses orbiting a distant red dwarf (Bennet et al. 2006). With these points in mind, we can put the results of our Gl 876 campaign in a broader context. A ground-based (and “fiscally viable”) photometric network such as Transit-
search, especially in collaboration with a dedicated bank of
telescopes, can capably monitor individual M dwarfs
to search for transits of terrestrial-sized planets. Owing
to the intrinsic long-term variability of M dwarfs, candi-
date planets would have to be identified on the basis
of a full transit signature in a single time-series.

A 0.1 $M_\odot$ M dwarf has $R_\ast/R_\odot \sim 0.1$, $T_{\text{eff}} \sim 2750$K,
and $L_\ast/L_\odot \sim 5 \times 10^{-5}$; a habitable planet that receives
an Earth-equivalent flux from the star thus needs to or-
bit at a distance of just 0.022 AU, which corresponds to
an orbital period of 3.85 days. An Earth-like planet with such a period would be rotationally synchronized to the
red dwarf, and in the absence of any significant pertur-
bating bodies, its orbit would be almost perfectly circular.
Interestingly however, simulations show that habitability is
unlikely to be adversely affected by a spin-orbit period
synchronization. Joshi, Haberle, & Reynolds (1997) used a
global climate model to investigate how the Earth’s cli-
mate would respond if the Earth were tidally locked to the
Sun, and found that Earth remains habitable in this
configuration – at 1 AU, and perhaps throughout the
habitable zone.

The $M = 7.5 M_\odot$, $P = 1.9379$ d companion to Gl 876 demonstrates that it is not unreasonable to expect
terrestrial-mass bodies on short-period orbits of 0.1 $M_\odot$
stars. Montgomery & Laughlin (2006) have carried out accretion simulations with the Wetherill-Chambers
method (Wetherill 1996, Chambers 2001) that model the
accretion of terrestrial-mass planets in short-period or-
bits about M dwarfs. These simulations provide further
evidence that terrestrial-mass planets will commonly
form in the desired short-period orbits.

If habitable planets do commonly form in orbit around
low mass M dwarfs, the chances of detecting and char-
acterizing them are surprisingly good. The transit of an
Earth-sized planet in front of an 11th magnitude 0.1
$M_\odot$ star. For a planet on a habitable 3.85 day
orbit, the transit will be relatively brief, $\sim 40$ minutes.
The a-priori geometric probability of observing such a
transit is $2\%$.

A 1% photometric dip is readily detectable. Amateur
astronomers who participate in the Transitsearch collabor-
ation routinely achieve detection thresholds of consid-
erably better than 1%, as evidenced by confirming detec-
tions of HD 149026b which has a transit depth of just
0.3%. Indeed, capable amateur observers have demon-
strated the photometric capability to detect the passage of a Mars-sized body in front of an 11th magnitude 0.1
solar mass red dwarf.

Inevitably one must ask how many suitable red dwarfs
are available on the sky as a whole. Even though the
lowest-mass M stars are the most common type of star,
they are also exceedingly dim. A dedicated 3m-class tele-
scope would be required to properly search the magni-
tude range V=16-18, where observations of the lowest-
mass red dwarfs begin to be plentiful (and indeed, many
0.1 $M_\odot$ stars within 10 parsecs still likely remain to
be discovered). In the meantime, however, we recom-
 mend that observers obtain high-cadence photometry of
nearby single stars listed in the RECONS catalog\(^\text{16}\) of
the 100 nearest stellar systems; these include Proxima

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\(^{16}\) maintained by T. Henry and collaborators at Georgia State University.

6. CONCLUSIONS

Our study of Gl 876 has produced several interesting
results. We have demonstrated that transits of planets b and c are not currently occurring, and we have thus
modestly constrained the parameter space available to
observationally allowed orbital configurations of the Gl 876 system. The absence of transits is consistent with
the dynamical study of Rivera et al. (2005) who find
that a co-planar system inclination $i \sim 50^\circ$ yields the
best fit to the radial velocity data. Our dynamical anal-
ysis indicates that when planetary transits in a strongly
interacting system similar to Gl 876 are eventually ob-
erved, then a tremendous amount of information will be
obtained. We look forward to the discovery of the first
such system.

We have also shown that a globally distributed net-
work of small-telescope observers can effectively provide
definitive photometric follow-up of known planet-bearing
low-mass stars. Our experience with Gl 876 indicates
that intensive photometric monitoring campaigns of in-
dividual, nearby M dwarfs constitute a tractable strategy
for planet detection. The Sun’s nearest low-mass stellar
neighbors should therefore be scrutinized very carefully
for transits by short-period terrestrial planets. A low-
budget survey of this type provides a small, but never-
theless non-negligible chance to discover a truly habitable
world from the ground, and within a year or two. Such a
detection would be a remarkable and exciting discovery.

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Fig. 1.— Uncertainty in the central transit time for planets “b” solid line and “c” dashed line. The vertical dashed lines delineate the time span of the Keck RV observations used to generate the co-planar fits that form the basis of our model photometric and RV curves. The vertical dotted line indicates the epoch for the fits (JD 2452490.0).
Fig. 2.— Model limb-darkened light curves during a predicted transit by planet "b" when it is near periastron (solid curves) and near apastron (dashed curves). The curves correspond to different assumed inclinations ($i = 90^\circ$, $89.9^\circ$, $89.8^\circ$, ..., $89.5^\circ$). The shallowest occur for $i = 89.5^\circ$. 
Fig. 3.— Model transit light curves for planet “c”, when it is near periastron (solid lines), and near apastron (dashed lines). Inclinations, $i = 90^\circ$ through $i = 89.0^\circ$ are shown in decrements of $0.1^\circ$. Planet “c”’s eccentricity $e \sim 0.22$ leads to a greater difference in transit depth and duration between periastron and apastron.
Fig. 4.— Three-planet RV model (dashed curve) with a superimposed model Rossiter curve (solid line) during a predicted transit by planet “c” near epoch JD 2453301.79. The observed Keck RV data is shown as the black filled-in circles with error bars.
Fig. 5.— Three-planet RV model (dashed curve) with a superimposed model Rossiter curve (solid line) during a predicted transit by planet “b” near epoch JD 2452446.14. Again, the observed Keck RV data is shown as the black filled-in circle with error bars.
Fig. 6.— Model $i = 89.6^\circ$ light curves for Gl 876 “b” and “c” superimposed on Hipparcos epoch photometry. None of the Hipparcos measurements were made near or during a predicted transit window.
Fig. 7.— Model $i = 89.3^\circ$ light curves for Gl 876 "b" and "c" superimposed on Fairborn Observatory photometry. Note that the intrinsic long-term variability for Gl 876 over a $\sim 1000$ day period is of order 0.05 magnitudes.
Fig. 8.— Model light curves for Gl 876 “c” superimposed on Fairborn Observatory photometry taken near three individual predicted transit windows. The solid lines correspond to model light curves arising from assumed inclinations running from $i = 90.0^\circ$ to $i = 89.0^\circ$. The light lines correspond to $i = 90^\circ$ model light curves arising from bootstrap fits in which the transit is $3\sigma$ early, $1\sigma$ early, and $1\sigma$ and $3\sigma$ late.
Fig. 9.— Left: Shankland 2003 data for “c”, this plate shows dynamical model light curves again for the same decrements of i, taken near JD 2452940.4381; relative photometry, which began in astronomical twilight (filled-in circles) Right: Dynamical model light curves for Gl 876 due to planet “c” for $i = 90.0^\circ$ through $89.0^\circ$ in $0.1^\circ$ decrements, taken near a predicted transit centered at JD 2453301.7879. The data were compiled, baselined and shifted to employ a mean magnitude of V=10.19, based on relative photometry obtained by AAVSO and TransitSearch (filled-in circles). The light lines correspond to $i = 90^\circ$ model light curves arising from bootstrap fits in which the transit is 3$\sigma$ early, 1$\sigma$ early, and 1$\sigma$ late and 3$\sigma$ late.
Fig. 10.— Dynamical model light curves for Gl 876 due to planet “b” for \( i = 90.0^\circ \) through 89.5° in 0.1° decrements, near a predicted transit centered at JD 2453300.3806. As with the previous figure, the data were baselined and shifted to employ a mean magnitude of \( V=10.19 \), based on relative photometry obtained by AAVSO and TransitSearch (filled-in circles). The light lines correspond to \( i = 90^\circ \) model light curves arising from bootstrap fits in which the transit is 3σ early, 1σ early, and 1σ late and 3σ late.
**TABLE 1**

**CO-P Planar Three-Planet \( i = 90^\circ \) Jacobi Parameters of the Gl 876 System**

| Parameter | Planet d | Planet c | Planet b |
|-----------|----------|----------|----------|
| \( m \) | \( 5.89 \pm 0.54 \) M\(_{\oplus} \) | \( 0.619 \pm 0.005 \) M\(_{\text{Jup}} \) | \( 1.935 \pm 0.007 \) M\(_{\text{Jup}} \) |
| \( P \) (d) | \( 1.93776 \pm 0.00007 \) | \( 30.340 \pm 0.013 \) | \( 60.940 \pm 0.013 \) |
| \( K \) (m s\(^{-1}\)) | \( 6.46 \pm 0.59 \) | \( 88.36 \pm 0.72 \) | \( 212.60 \pm 0.76 \) |
| \( a \) (AU) | \( 0.0208067 \pm 0.0000005 \) | \( 0.13030 \pm 0.00004 \) | \( 0.20783 \pm 0.00003 \) |
| \( e \) | 0 (fixed) | \( 0.2243 \pm 0.0013 \) | \( 0.0249 \pm 0.0026 \) |
| \( \omega \) (°) | 0 (fixed) | \( 198.3 \pm 0.9 \) | \( 175.7 \pm 6.0 \) |
| \( M \) (°) | \( 309.5 \pm 5.1 \) | \( 308.5 \pm 1.4 \) | \( 175.5 \pm 6.0 \) |
| Transit epoch JD | \( 2452490.756 \pm 0.027 \) | \( 2452517.633 \pm 0.051 \) |

\(^a\)Quoted uncertainties in planetary masses and semi-major axes do not incorporate the uncertainty in the mass of the star.