Highly Efficient Adsorption of Cd(II) onto Carboxylated Camelthorn Biomass: Applicability of Three-Parameter Isotherm Models, Kinetics, and Mechanism

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Abstract
A series of malonic acid treated camelthorn (MATC) sorbents were produced via the reaction of camelthorn biomass with malonic acid, and factors affecting the extent of modification were investigated, including malonic acid concentration, dehydration time and temperature. The optimum sorbent, by carboxylic acid content, was subsequently characterised for surface charge behaviour (pHPZC), surface chemical functionalities (FTIR), morphological structure (SEM), and available surface area. The sorbent was subsequently utilised for adsorption of Cd(II) ions from aqueous media, and parameters influencing adsorption at 30 °C, such as sorbent dose, initial solution pH, exposure time, metal concentration, were investigated. Isothermal analyses were performed using eight models, including two and three parameter equations, with appropriateness of fit assessed via non-linear regression analysis. The adsorption data indicated that the Langmuir model gives the most appropriate fit to experimental curves, with the models ordered as Langmuir > Hill > Toth > Sips > Jossens > Khan > Redlich-Peterson > Freundlich. The highest uptake (qmax) of 582.6 mg g⁻¹ was determined at pH 6. The Freundlich constants, KF and n, at 30 °C were found to be 24.94 mg g⁻¹ and 2.33, respectively. The value of n (2.33), being in the range 0–10, indicates that adsorption of Cd(II) ions onto malonic acid treated camelthorn biomass is favourable. Evaluation of a series of kinetic models, allowed elucidation of the adsorption mechanism, as a pseudo-second order model gave the most appropriate fit, indicating that chemisorption processes are involved. Cd(II) ions adsorption onto MATC is enhanced by a higher level of active surface sites but was show to be independent of surface area. The work presented here indicates that this sorbent offers effective adsorption potential for Cd(II) ions from water, with potential in wastewater processing.

Keywords Camelthorn · Chemical modification · Isotherm models · Kinetic models

Introduction
Remediation of heavy metal species from industrial and mine wastewaters is a key challenge in reducing related water and flora contamination. Cadmium has attracted significant attention from those working in environmental remediation as a result of its high toxicity in the ionic form, which enters the environment from a number of industries [1, 2]. Cadmium is known to bioaccumulate, being linked to renal and pulmonary issues, bone lesions, cancer, and hypertension [3]; and the World Health Organisation has mandated an upper allowable level of 3.0 μg L⁻¹ of Cd(II) ions in drinking water [4]. Cadmium is easily absorbed by plants and crops such as wheat and rice. It has a strong ability to become enriched, and easily enters the body through the food chain, resulting in a hazard to human health through water, air, and plants [5]. A number of methods have been proposed for remediation of heavy metal ions from industrial effluents such as neutralisation, ion exchange, solvent extraction, photochemical degradation, electrochemical degradation, membrane separation, reverse osmosis, precipitation and adsorption [5–11], while these have been proven to
be efficient, they are also expensive; by contrast adsorption provides an efficacious method for the remediation of heavy metal ions from water [12].

Activated carbon is often used; an efficient sorbent it is, however, also costly, therefore, a need exists for cost-effective alternatives, which has motivated research into new sorbent materials, particularly those sourced from waste materials. Such a class of materials is those with lingo-cellulosic character and agricultural by-products have seen increased attention for such applications [13–16]. It has been shown that chemical modification, including incorporation of surface moieties and chemical coupling, can improve sorbent behaviour of these materials towards heavy metals [17–20].

This work aims to improve the ability of camelthorn to adsorb Cd(II) ions from water, by treatment of prepared camelthorn biomass with malonic acid to obtain malonic acid-treated camelthorn (MATC), with subsequent determination of the capacity and mechanism for adsorption of Cd(II) from water, evaluated through the fit of selected isothermal and kinetic models to experimentally obtained data, assessed via non-linear regression.

Materials and Methods

Materials

Camelthorn biomass utilised in this study were acquired from the Sebha desert, Libya. The lingo-cellulosic materials of camelthorn is found within the root content of this plant, hence, these were separated from the remaining organic matter, and washed with a plentiful supply of purified water to eliminate any surface particles, before subsequent drying at 80 °C for 10 h; grinding and sieving of the resulting material, gave a final product with particle size 50–120 μm. Laboratory grade chemicals were supplied by Merck, Germany: Cd(CH₃COO)₂, EDTA, CH₂(COOH)₂, CH₃COOH, Na₂CO₃, (CH₃)₂CO, NaOH, HNO₃, and C₂H₅OH.

Preparation of the Sorbent

MATC sorbents were prepared by adding 2 g of camelthorn powder to a known mass of malonic acid dissolved in water. Stirring produced a homogeneous paste, which was dried at 100–150 °C, before cooling to ambient temperature. An ethanol/water mixture (80:20) was used to wash the cooled sample to remove unreacted/unwanted species. The resulting refined material was dried at 80 °C for 6 h. Under high temperatures, malonic acid converts to the anhydride form - this reacts with hydroxyl moieties, such as those on the camelthorn residue surface to obtain the MATC sorbent, as shown in Scheme 1:

![Scheme 1 Reaction of camelthorn with malonic acid, at elevated temperatures, producing malonic acid treated camelthorn sorbents](image)

Batch Adsorption Studies

0.03 g of sorbent was added to 100 cm³ of Cd(CH₃COO)₂ solution (0.1–1 g L⁻¹); initial pH was altered by dropwise addition of 0.1 M HNO₃ or NaOH; with the solution mixed (150 rpm at 30 °C) before filtering to separate the sorbent and bulk solution. Pre- and post-adsorption Cd(II) ion concentrations were determined via titration with 0.0005M EDTA solution, and the equilibrium uptake of Cd(II), qₑ (mg g⁻¹), determined using Eq. 1 and percentage removal calculated using Eq. 2.

\[
qₑ = \frac{V(C₀ - Cₑ)}{W} \quad (1)
\]

Removal % = \(
\frac{C₀ - Cₑ}{C₀} \times 100
\) \quad (2)

where \(C₀\) and \(Cₑ\) (mg L⁻¹) are initial and equilibrium Cd(II) ion concentration, \(W\) (g) is mass of sorbent used, and \(V\) (L) is 0.1 L, i.e. Cd(II) ion solution volume.

Carboxylic Acid Content

The quantity of carboxylic acid moieties of the sorbents were determined by adding 0.2 g to 50 cm³ of 0.03 N NaOH. Several systems were created and allowed to equilibrate overnight at ambient temperature, after which the amount of carboxylic acid moieties were evaluated via titration 0.01N HCl and phenolphthalein indicator [21]. The quantity of carboxylic acid moieties of each sorbent was determined using:

\[
[COOH] \cdot \frac{\text{meq}}{100 \text{g sample}} = \frac{(V₀ - V₁) \cdot 0.01}{W} \times 100 \quad (3)
\]
where \( V_0 \) is HCl volume \( (\text{cm}^3) \) consumed in a blank experiment, \( V_l \) is HCl volume \( (\text{cm}^3) \) consumed by the sorbent, and \( W \) is mass of sorbent used \((\text{g})\).

**Characterisation of the Sorbent**

Samples of camelthorn, MATC and MATC with Cd(II) ions adsorbed were characterised using FTIR (~ 2–10 mg of sorbent in 300 mg KBr to form discs analysed using a Perkin-Elmer Spectrum 1000 spectrometer, 400–4000 cm\(^{-1}\), interval 1 cm\(^{-1}\) and 120 scans) allowing assignment of vibrational frequencies associated with functional groups present on the sorbent surface, and of any interactions between the adsorbed Cd(II) ions and the sorbent surface. Sorbent surfaces were coated with chromium on carbon tape and imaged at 1000× magnification (TESCAN CE VEGA 3 SBU). Energy-dispersive X-ray (EDX) patterns were obtained to confirm the presence of metal ions on the surface post-adsorption (Oxford Instruments EDX attached to JEOL-JSM-5600). Porous characteristics were determined using O\(_2\)-free N\(_2\) adsorption at 77 K (Autosorb I, Nova 2000, Quantahrome Instruments); isothermal data was analysed to determine surface area \([22]\), mesopore characteristics \([23, 24]\), and average pore width and pore size distribution \([25]\). Point of zero charge (pH\(_{\text{PZC}}\)) was determined by adding 100 mg of the sorbent to each of a series of flasks containing 100 cm\(^3\) of 0.01 N NaCl, in which the initial pH was adjusted (pH 2 to 12), using 0.01 N HCl or 0.01 N NaOH. Initial pH and pH after 48 hr contact were recorded and plotted; the intersection denoting pH\(_{\text{PZC}}\).

**Error Analysis**

 Appropriateness of the series of kinetic and isotherm models applied to the experimental data acquired in this work was determined using the absolute relative error (ARE) and coefficient of determination \((R^2)\) (Eqs. 4 and 5) \([26, 27]\), using the criteria of ARE close to 0 and \(R^2\) close to 1.

\[
R^2 = 1 - \frac{\sum_{i=1}^{n} (q_{e,\text{exp}} - q_{e,\text{cal}})^2}{\sum_{i=1}^{n} (q_{e,\text{exp}})^2 - \left[\frac{\sum_{i=1}^{n} (q_{e,\text{exp}})^2}{n}\right]^2} \tag{4}
\]

\[
\text{ARE} = \frac{1}{n} \sum_{i=1}^{n} \left| \frac{q_{e,\text{exp}} - q_{e,\text{cal}}}{q_{e,\text{exp}}} \right| \tag{5}
\]

where \( n \), \( q_{e,\text{exp}} \) and \( q_{e,\text{cal}} \) are the range of input data, experimental, and calculated uptake of Cd(II) ions, respectively.

**Results and Discussion**

**Sorbent Characterisation**

The FTIR spectra obtained for native camelthorn (Fig. 1a), exhibited an absorption band at 3323 cm\(^{-1}\), due to the stretching vibration of hydrogen-bonded alcoholic and phenolic –OH groups; a weak band at 2915 cm\(^{-1}\), which is most probably due to C–H bond stretching vibrations \([28]\); a peak at 1625 cm\(^{-1}\), ascribed to C=C stretching \([29]\); weak bands between 1400 and 1500 cm\(^{-1}\) indicating aromatic ring C-C bonds; a relatively wide band at 1000 cm\(^{-1}\), related to the presence of C-O groups \([30]\). From Fig. 1b, the additional absorption peaks for MATC are observed at 1729 cm\(^{-1}\), assigned to stretching vibrations of the newly formed ester carbonyl groups resulting from modification of camelthorn with malonic acid; and the characteristic peak at 1443 cm\(^{-1}\) for the absorption of -OH bending vibrations in -COOH. This evidence indicates the successful modification of camelthorn with malonic acid \([31]\) to create new ester moieties on the surface. Figure 1c shows the FT-IR spectra of MATC loaded with Cd(II) ions, as obtained post-adsorption. In comparison with the native camelthorn and MATC sorbents (Fig. 1a, b), the intensities of –OH, C=O, and C–O groups are increased, which indicates their significant role in the adsorption of Cd(II) ions onto the surface of MATC, and Cd(II) adsorption onto MATC may involve a complexation mechanism. It should be noted that while the FTIR results provide an indication of the groups involved in attracting Cd(II) ions to the sorbent surface, they do not provide any quantitative analysis or information about the level of affinity of the metal to the functional groups present in the sorbents.
Figure 2a shows the surface morphology of MATC, and this image reveals a cluttered and agglomerated material with pores present. After metal adsorption, the pores present on the MATC surface were occupied with Cd(II) ions, resulting in the formation of a non-uniform and rough surface. The Cd(II) deposited in the surface pores is in the form of aggregates, thus multi layers of Cd metal cover the modified camelthorn surface (Fig. 2b). This morphological change confirms the presence of Cd metal on the sorbent surface post-adsorption. Additional confirmation is provided by the EDX spectra of MATC loaded with Cd(II) ions, presented within the chart of Fig. 2c, with the sharp peaks corresponding to the presence of elemental cadmium.

Figure 3a presents the nitrogen adsorption–desorption isotherms obtained for MATC at −196 °C, while the pore size distribution is shown in Figure 3b. The sorbent showed a BET surface area of 1.3 m²g⁻¹ and a pore volume of 2 × 10⁻³ cm³g⁻¹. A hysteresis loop can be observed in the adsorption-desorption profiles, which, according to the IUPAC classification, is associated with a Type IV isotherm.
suggesting mesoporous character [32]. This observation is supported by the distribution shown in Figure 3b, which indicates that the average pore size is ~6 nm and that most of the surface pores fall within the mesoporous structure range (2–50 nm), which are capable of admitting not only metal ions, but also large sized dye molecules [33].

Factors Affecting Modification of Camelthorn Biomass

Effect of Malonic Acid Concentration

Figure 4 shows the extent of modification of camelthorn biomass, expressed as meq-COOH/100 g sorbent, as a function of malonic acid concentration. The carboxylic acid content increases markedly, from 70 to 258.8 meq/100 g sorbent, with increasing malonic acid concentration (2.4 to 14.4 mmol L\(^{-1}\)); further increases in malonic acid concentration resulted in a plateau at a maximum level of functionalisation. The increase in carboxylic acid content may be attributed to the greater availability of malonic acid molecules within the proximity of the camelthorn cellulose macromolecules with increasing malonic acid concentration, which is converted to the corresponding anhydride through dehydration under the effect of heat (Scheme 1). The anhydride obtained reacts with the cellulose hydroxyl groups of camelthorn to produce the MATC sorbent. Functionalisation happens at the immobile hydroxyl moieties of the sorbent surface, hence, increased malonic acid availability is essential for increased reaction and conversion of these surface groups.

Effect of Dehydration Temperature

Figure 5 shows the effect of dehydration temperature on carboxylic acid content of MATC, which increases from 120.8 to 258.8 meq/100 g sorbent (100 to 140 °C) before a decrease at higher temperatures (> 140 °C). At temperatures in the range 100–140 °C, malonic acid converts of the anhydride analogue (Scheme 1), and reaction kinetics will be increased with thermal stimulation; above this temperature, catalytic effects (decarboxylation) may impede reaction, and cellulosic material may be reduced to ash at very high temperatures (> 150 °C).
Effect of Reaction Time

Figure 6 shows the influence of reaction time on carboxylic acid content of MATC, at 140 °C and reaction times in the range 30–180 min. Figure 6 shows an increase from 150 to 258 meq/100 g sorbent for short to medium increasing reaction times, before a subsequent decrease at longer reaction times. These longer reaction intervals may be attributed to catalytic effects leading to the formation of carboxylic acid moieties at increased exposure times.

Factors Affecting Adsorption

Effect of Solution pH

Figure 7a shows the point of zero charge (pH\textsubscript{PZC}) data for the surface of the MATC sorbent, allowing the pH at which the surface of MATC has neutral charge to be determined. At a solution pH higher than pH\textsubscript{PZC}, the surface will be mainly negatively charged, and mainly positively charged if a solution pH is lower than pH\textsubscript{PZC} \[19, 34\], hence, the pH\textsubscript{PZC} gives information about the electrostatic interaction between the adsorbate and the sorbent surface \[35\]. The pH\textsubscript{PZC} of MATC was determined as 4.0, indicating that it is acidic in nature; when the pH value of the solution is higher than pH\textsubscript{PZC}, the charge of the MATC surface will be negative and favours the binding of cations, and when the pH value of the solution is lower than the pH\textsubscript{PZC}, the surface charge of the sorbent will be positive and, therefore, the adsorption of cations is unlikely \[36\].

Fig. 5 Effect of dehydration temperature on extent of modification expressed as meq -COOH/100 g sample of malonic acid treated camelthorn. Reaction conditions: mass of camelthorn biomass: 2 g; particle size range: 50–125 μm; reaction time: 2 h; malonic acid concentration: 14.4 mmol L\textsuperscript{-1}

Fig. 6 Effect of reaction time on extent of modification expressed as meq -COOH/100 g sample of malonic acid treated camelthorn. Reaction conditions: mass of camelthorn biomass: 2 g; particle size range: 50–125 μm; malonic acid concentration: 14.4 mmol L\textsuperscript{-1}; dehydration temperature: 140 °C

Fig. 7 (a) pH\textsubscript{PZC} of malonic acid treated camelthorn at room temperature; (b) Influence of pH on adsorption capacity of Cd(II) ions onto MATCat 30 °C. Reaction conditions: adsorbent dose: 0.3 g L\textsuperscript{-1}; Cd(II) ion concentration: 300 mg L\textsuperscript{-1}; contact time: 2 h; adsorption temperature, 30 °C; particle size range, 50–125 μm; carboxyl content, 258.5 meq/100 g sample
Cd(II) ions are known to precipitate from solution at pH values greater than 7, thus, the pH was kept below 7 in all experiments within his study. The relationship between pH and adsorption capacity of Cd(II) ions onto MATC is presented in Figure 7b, as a function of increasing pH. As pH increases from 2 to 6, there is an increase in Cd(II) uptake from 22 to a maximum value of 175 mg g⁻¹ for this system. At lower pH, more hydrogen ions (protons) are available within the solution, leading to strong competition with metal ions towards the active sites of the sorbent [14, 37]; at such levels there will also be electrostatic repulsion between the more charged surface of the sorbent and the charged Cd(II) ions. At higher pH, the influences of competition and electrostatic repulsion are reduced, and adsorption is enhanced, as observed here. Such behaviour has been observed previously for Cd(II) adsorption on pine sawdust [19]. Another possible reason for increasing adsorption capacity with increasing pH from 3-6 can be attributed to the following reactions:

\[
2\text{Camelthorn} - \text{COOH} \Leftrightarrow 2\text{Camelthorn} - \text{COO}^- + 2H^+ \quad (6)
\]

\[
2\text{Camelthorn} - \text{COO}^- + \text{Cd}^{2+} \Leftrightarrow (\text{Camelthorn} - \text{COO})_2\text{Cd} \quad (7)
\]

Equation 6 represents deprotonation, the first stage in ion exchange, while Eq. 7 represents the adsorption of Cd(II) ions onto the deprotonated MATC. The pHₚzC of TMCC was determined as 4.0, which denotes the point at which a neutral charge is obtained and indicating an acidic nature for the surface of the TMCC adsorbent. The optimum pH for MATC to adsorb Cd(II) is 6.0 (Figure 7a) which is higher than the pHₚzC. This leads to a predominantly negative sorbent surface, which may lead to electrostatic attraction (ion exchange) between the Cd(II) ions and negatively charged surface [38].

**Effect of Sorbent Dose**

The effect of sorbent dose on adsorption capacity and percentage removal of Cd(II) ions onto MATC were studied at pH 6 (sorbent concentrations: 1–10 g L⁻¹, initial metal ion concentration: 300 mg L⁻¹). It is clear from Fig. 8 that the removal of Cd(II) ions increased from 15 to 98% with increasing sorbent concentration (0.3 to 10 g L⁻¹), which may be due to the availability of more adsorption sites [39]. In contrast, uptake (qₑ) decreased with increasing sorbent dosage, which may be due to overcrowding of sorbent particles in solution and competition between metal ions for active sites.

**Influence of Time**

The influence of exposure time on adsorption capacity of Cd(II) ions onto malonic acid treated camelthorn at 30 °C is shown in Fig. 9, with adsorption increasing rapidly to 145 mg g⁻¹ at 5 min, with only a small increase between 5 and 20 min. Beyond 20 min, adsorption remains constant indicating that the equilibrium state has been achieved. The highest uptake of Cd(II) ions onto MATC was 175 mg g⁻¹. The initial, rapid adsorption of Cd(II) ions could be due to the presence of active surface sites on the sorbent; after which such sites are occupied, which reduces Cd(II) adsorption [30]. The reported saturation at 20 min for Cd(II) adsorption onto MATC is quicker than the 60 min timeframe, previously reported for Cd(II) ion adsorption on modified sawdust [19].
Influence of Adsorbate Concentration Under Isothermal Conditions

Isotherm models relate adsorption uptake, $q_e$ (metal adsorption per unit weight of sorbent), to the equilibrium adsorbate concentration within the bulk fluid phase, $C_e$, and several models, with either two or three parameters, have been reported to describe experimental data of adsorption isotherms. In this study, eight such models were selected to describe the adsorption equilibrium of Cd(II) onto MATC.

The Langmuir model [40] is generally utilised for pollutant adsorption from solution and is founded on the key assumptions that adsorption is limited to monolayer formation, adsorption only occurs at surface sites in the energetically homogeneous sorbent surface, and molecules adsorbed on neighbouring sites do not interact. The model is represented by:

$$q_e = \frac{K_L \cdot C_e}{1 + a_L \cdot C_e}$$  \hspace{1cm} (8)

$K_L$ (L g$^{-1}$) and $a_L$ (L mg$^{-1}$) are isotherm model constants, and $K_La_L$ is the maximum capacity ($q_{\text{max}}$). $C_e$ is the equilibrium adsorbate concentration, measured in mg L$^{-1}$, and $q_e$ is normalised uptake of Cd(II) ions (mg g$^{-1}$).

The Freundlich model was developed for multilayer systems with a logarithmic distribution of surface site energies across the heterogeneous surface. This model is based on the fact that the higher affinity sites are occupied initially and that total uptake is summed for all sites. The model also assumes multilayer adsorption on the surface and predicts infinite adsorption uptake. The model is expressed by [41]:

$$q_e = K_R \cdot C_e^{1/n}$$  \hspace{1cm} (9)

$q_e$ and $C_e$ are as previously defined, $K_R$ and $n$ are Freundlich constants related to uptake capacity and likelihood, respectively.

The Redlich–Peterson model [42], featuring aspects from Freundlich and Langmuir isotherms, favours multilayer formation. An empirically derived model, it exhibits Henry’s behaviour at dilute concentrations and reduces to the Freundlich model at high ionic strengths. The model is represented by:

$$q_e = \frac{k_R \cdot C_e}{1 + a_R \cdot C_e}$$  \hspace{1cm} (10)

$q_e$ and $C_e$ are as previously defined, $k_R$ (L g$^{-1}$) and $a_R$ are the constants of adsorption, the exponential term $g$ (0 to 1), means that Equation 10 reduces to the Langmuir model at unity, and, as $g$ tends to 0, Eq. 10 reduces to Henry’s law, and Henry’s constant is given by $k_R/(1+a_R)$.

Heterogeneous adsorption systems can also be described by the Toth model [43]; which is again a modified form of the Langmuir equation, satisfying both dilute and concentrated boundaries. The model is expressed by:

$$q_e = \frac{K_T \cdot C_e}{(a_T + C_e)^{1/t}}$$  \hspace{1cm} (11)

$q_e$ and $C_e$ are as previously defined, $K_T$ is the Toth isotherm constant, $a_T$ is the maximum uptake, and $t$, in the term $1/t$, indicates the level of heterogeneity within the sorbent, where unity results in the model reducing the Langmuir model, i.e. a homogeneous system.

Another combinatorial model, the Sips model [44] is founded on the presence of a heterogeneous surface; the model is expressed by:

$$q_e = \frac{k_s \cdot C_e^{n_H}}{1 + a_s \cdot C_e^{n_H}}$$  \hspace{1cm} (12)

$q_e$ and $C_e$ are as previously defined, $k_s$ (L g$^{-1}$) and $a_s$ (L mg$^{-1}$) are the Sips isotherm constants, and $n_H$ is an exponent. The Sips isotherm reduces to the Freundlich model for dilute systems, while predicting completion of a single adsorption layer, as expected from the Langmuir model, for concentrated systems.

The Hill model [45] is founded on cooperative processes and assumes a homogeneous surface is present, the model is described by:

$$q_e = \frac{q_{\text{SH}} \cdot C_e^a}{K_D \cdot C_e^a}$$  \hspace{1cm} (13)

$q_e$ and $C_e$ are as previously defined, $k_D$ is the Hill constant (mg), $n_H$ is the Hill cooperativity coefficient, and $q_{\text{SH}}$ indicates maximum uptake (mg mg$^{-1}$).

Khan [46] proposed a common model for adsorption from dilute dual adsorptive systems using pure system data, however, the model can also be applied in this case. The general Khan isotherm model for a single solute is represented by:

$$q_e = \frac{q_{\text{max}} b_k C_e}{1 + b_k C_e^a}$$  \hspace{1cm} (14)

$q_e$ and $C_e$ are as previously defined, $a_K$ is an exponent and $b_k$ is the Khan isotherm constant.

Jossens [47], again proposed a model based on a distribution of energies across the sorbent surface, i.e. a heterogeneous surface, controlling adsorbate-adsorbent binding. The model is represented by:

$$q_e = \frac{K_f C_e}{(1 + J C_e^g)}$$  \hspace{1cm} (15)
\( q_e \) and \( C_e \) are as previously defined, \( K_J \) is the Jossens isotherm model constant, corresponding to Henry’s constant; \( J \) is the Jossens model constant, and \( \beta \) is the Jossens model exponent, which is characteristic of the sorbent and is independent of temperature (Tables 1, 2).

### Table 1: Isotherm constants of two-parameter models for Cd(II) ion adsorption onto malonic acid treated camelthorn biomass at 30 °C

| Isotherm Model | Parameter | Value | Error Analysis | Value |
|---------------|-----------|-------|----------------|-------|
| Langmuir     | \( a_L \) | 0.0035 L mg\(^{-1}\) | \( R^2 \) | 0.9998 |
|              | \( q_{\text{max}} \) | 1000 mg g\(^{-1}\) | ARE | 0.1238 |
|              | \( k_L \) | 2.035 L g\(^{-1}\) |       |       |
| Freundlich   | \( N \) | 2.333 | \( R^2 \) | 0.9961 |
|              | \( K_F \) | 24.935 mg g\(^{-1}\) | ARE | 0.6737 |

### Table 2: Isotherm constants of three-parameter isotherm models used to fit data for Cd (II) ion adsorption onto malonic acid treated camelthorn biomass at 30 °C

| Isotherm Model     | Parameter | Value     | Error Analysis | Value     |
|--------------------|-----------|-----------|----------------|-----------|
| Redlich-Peterson   | \( k_g \) | –0.0110 | \( R^2 \) | 0.9965 |
|                    | \( \alpha_R \) | 24.60 | ARE | 0.6712 |
|                    | \( g \) | 0.4335 |       |       |
| Sips               | \( K_s \) | 12.85 | \( R^2 \) | 0.9969 |
|                    | \( \alpha_s \) | 0.0101 | ARE | 0.4395 |
|                    | \( \beta_s \) | 0.5298 |       |       |
| Toth               | \( k_t \) | 11.81 | \( R^2 \) | 0.9982 |
|                    | \( \alpha_T \) | 0.0800 | ARE | 0.4306 |
|                    | \( 1/t \) | 0.4514 |       |       |
| Khan               | \( q_{\text{in}} \) | 2.457 | \( R^2 \) | 0.9967 |
|                    | \( b_K \) | 197.1 | ARE | 0.6568 |
|                    | \( \alpha_K \) | 0.5670 |       |       |
| Jossens            | \( K_J \) | 10.77 | \( R^2 \) | 0.9967 |
|                    | \( J \) | 0.3253 | ARE | 0.4940 |
|                    | \( B \) | 0.6060 |       |       |
| Hill               | \( q_{30} \) | 500 | \( R^2 \) | 0.9986 |
|                    | \( n_H \) | 1.211 | ARE | 0.3122 |
|                    | \( K_{\text{fp}} \) | 637.0 |       |       |

### Table 3: Comparison of adsorption capacities of various sorbents for Cd(II) ions

| Adsorbent                                      | Adsorption capacity (mg g\(^{-1}\)) | Removal time (min) | Reference |
|------------------------------------------------|-------------------------------------|--------------------|-----------|
| Sulfuric acid treated cashew nut shell (STCNS) | 436.7                               | 30                 | [48]      |
| Esterified spent grain (ESG)                    | 473.93                              | 15                 | [49]      |
| Wood Apple Shell                                | 32.7                                | 30                 | [50]      |
| Commercial activated carbon (CGAC)              | 17.23                               | 180                | [51]      |
| Sawdust treated maleic acid                     | 180.4                               | 45                 | [19]      |
| Malonic acid modified camelthorn                | 582.6                               | 20                 | Present study |

### Isotherm Modelling

Minimisation of the errors obtained in a comparison of experimental and calculated data was performed using two error functions for all models utilised in this study. The error functions used were Average Relative Error (ARE) and the coefficient of determination \( (R^2) \), and these were optimised by non-linear regression to attenuate the function errors between the results obtained experimentally in this study and the values determined from the isotherm models applied here. The data in Table 3 also indicate that MATC has the lowest removal time compared with comparator sorbents. Figure 10 shows the experimental isotherm curves acquired in this study and the calculated curves obtained for the isotherm models applied to fit these data, namely the Langmuir and Freundlich models, which are each based on two parameters. The constants obtained for each fit for these two models, as well as the values obtained for error analyses of the fits, are shown in Table 1. It is known that \( 1/n \), from the Freundlich model, indicates the favourability of the adsorption process. In this study, the value obtained was 2.333 (Table 1), which also falls within the range 0 < \( n \) < 10, both of which suggest that adsorption of Cd(II) ions onto MATC is expected [31]. The data presented in Table 1 demonstrate that the Langmuir model provides the most appropriate description of the experimental data, suggesting that adsorption within the current system is limited to monolayer formation on a homogeneous surface, which agrees with previous results reported for Cd(II) ions adsorption on aminated hydroximoyl camelthorn [20]. Figures 10 and 11 show comparisons between the experimental and theoretical data for all models studied and parameters determined for each of the fits are presented in Tables 1 and 2. From the results obtained, it is evident that the Langmuir model gives the most appropriate fit to experimental curves, with the models ordered as Langmuir > Hill > Toth > Sips > Jossens > Khan > Redlich-Peterson > Freundlich. The maximum uptake for Cd(II) ions onto MATC, as determined using the Langmuir model, is 582.6 mg g\(^{-1}\). Table 3 shows that the malonic acid-treated camelthorn synthesised in this
work demonstrates enhanced adsorption capacity for Cd(II) ions from water systems in comparison with esterified spent grain (473.93 mg g⁻¹) and a number of other sorbents [19, 48–51].

**Adsorption Kinetics**

It is essential that a high equilibrium adsorption capacity for a given system is obtained in tandem with appropriate kinetic parameters if these materials are to be considered as candidates for water remediation. Here, five kinetic models were used to analyse data obtained for adsorption for Cd(II) ions on MATC with respect to time. As outlined above, two error functions were utilised to evaluate the goodness of fit for each model applied to the data acquired in this study (ARE and R²).

The pseudo-first-order model, being founded on a physical process under diffusion control, is represented by [52]:

\[ q_t = q_e [1 - \exp(-k_1t)] \]  

(16)

where \( q_t \) is the uptake, at time \( t \) (min), of Cd(II) ions (mg g⁻¹), \( q_e \) is the equilibrium uptake of Cd(II) ions (mg g⁻¹), \( k_1 \) is the rate constant (min⁻¹). Values obtained for \( q_e \) and \( k_1 \) are given in Table 4 with the associated error analysis.

The pseudo-second order kinetic model was derived on the basis that the adsorbate experiences physicochemical interaction with the adsorbent, i.e. the two species share electrons; the model is represented by [53]:

\[ q_t = \frac{k_2 q_e^2 t}{1 + k_2 q_e t} \]  

(17)

where \( q_t \), \( q_e \) are as previously defined, and \( k_2 \) (g mg⁻¹ min⁻¹) is the rate constant. Values obtained for \( q_e \) and \( k_2 \) are given in Table 4 with the associated error analysis.

It is necessary, in addition to the models described above, to consider the intra-particle diffusion model, to provide insight into the diffusion mechanism of the system. The model is represented by [54]:

\[ q_t = k_{id} t \]  

(18)

\[ q_e \] is the equilibrium uptake of Cd(II) ions (mg g⁻¹), \( k_{id} \) is the intra-particle rate constant (mg g⁻¹ min⁻¹). Values obtained for \( k_{id} \), \( q_e \) and \( C \) are given in Table 4 with the associated error analysis.

### Table 4 Kinetic model data obtained for selected models used to fit data for Cd(II) ions adsorption onto malonic acid treated camelthorn biomass at 30 °C

| Isotherm Model      | Parameter | Value | Error Analysis | Value |
|---------------------|-----------|-------|----------------|-------|
| Pseudo-first-order  | \( q_e \) | 174.6 | R²             | 0.9974|
|                     | \( k_1 \) | 0.3435| ARE            | 0.2852|
| Pseudo-second-order | \( q_e \) | 195.3 | R²             | 0.9985|
|                     | \( k_2 \) | 0.0014| ARE            | 0.2209|
| Intra-particle      | \( k_{id} \) | 7.247 | R²             | 0.9960|
|                     | \( C \)    | 125.9 | ARE            | 0.3711|
| Bangham             | \( q_e \)  | 183.4 | R²             | 0.9984|
|                     | \( k_0 \)  | 0.6126| ARE            | 0.2452|
|                     | \( n \)    | 0.4271|                |       |
| Elovich             | \( \alpha \) | 114844.4 | R²      | 0.9963|
|                     | \( B \)    | 0.0744| ARE            | 0.3244|
\[ q_t = k_{\text{id}} t^{0.5} + q_e \] (18)

\[ t, q_t, q_e \text{ are as previously defined, } k_{\text{id}} \text{ (mg g}^{-1}\text{min}^{-1/2}) \text{ is the rate constant. It has previously been reported that the trend obtained graphically for } q_t \text{ vs. } t^{1/2} \text{ consists of a series of steps, which each contribute to overall control of the process. An Initial curve indicates bulk diffusion, after which a linear section denotes intra-particle diffusion; the final plateau is achieved at equilibrium [55, 56]. Values obtained for } C \text{ and } k_{\text{id}} \text{ and the associated error analysis are given in Table 4.} \]

Pore-diffusion as rate-control can be determined using Bingham’s model [57], as represented by:

\[ q_t = q_e \left[ 1 - \exp \left( -k_b t^n \right) \right] \] (19)

\[ t, q_t, q_e \text{ are as previously defined, and } k_b \text{ is the rate constant. Values obtained for } q_e, k_b, \text{ and the associated error analysis are given in Table 4.} \]

Finally, the Elovich model [58] is represented by:

\[ q_t = \left( \frac{1}{\beta} \right) \ln (\alpha t) \] (20)

\[ \alpha \text{ (mg g}^{-1}\text{min}^{-1}) \text{ is initial rate of adsorption and } \beta \text{ (g mg}^{-1}\text{L}^{-1}) \text{ is made up of contributions from uptake within the system and chemisorption related activation energy. Values obtained for } \alpha \text{ and } \beta \text{ and the associated error analysis are given in Table 4.} \]

Fits for the five kinetic models used in this study are shown in Fig. 12; the results (Table 4) show that the models can be ordered: pseudo-second-order > Bangham > pseudo-first-order > Elovich > intra-particle for goodness of fit to data acquired within this study, indicating chemical control of the process.

**Adsorption Mechanism**

The removal of Cd(II) ions from solution onto MATC can be described by three mechanisms. The first is exchange of Cd(II) ions with H\(^+\) associated with the carboxylic acid moieties present in MATC, which result from the thermal treatment of camelthorn biomass with malonic acid, this is consistent with the data obtained from pH and pH\(_{\text{ZPC}}\). The second is intra-particle diffusion control involving (a) movement of the adsorbate from bulk solution to the sorbent surface, (b) diffusion of the adsorbate through the boundary layer to the sorbent surface, (c) adsorption of Cd(II) ions on sorbent surface active sites, and (d) intra-particle diffusion of the Cd(II) ions into the internal pores of the sorbent. Finally, chelation (complexation) may occur between the Cd(II) ions, which are electron-accepting in character, and electron-donating species, e.g. oxygen-rich moieties of the sorbent surface (Scheme 2) [19].

**Conclusions**

Camelthorn biomass were modified by thermally-driven reaction with malonic acid to create malonic acid treated camelthorn (MATC) sorbents. The process was shown to be affected by malonic acid concentration, dehydration time and temperature, allowing an optimal sorbent to be obtained, which was characterised for textural, morphological and chemical structure. The sorbent showed a rough aggregated surface with little available surface area (1.3 m\(^2\) g\(^{-1}\)), and increased active surface groups upon reaction with malonic acid. MATC sorbents were utilised for adsorption of Cd(II) ions from water; the results indicate that uptake of Cd(II) ions on MATC was affected by pH, sorbent concentration, exposure time, and initial metal ion concentration. Isothermal analysis using eight isotherm models with either two or three parameters, showed the Langmuir model to provide the most appropriate description of the isothermal data, allowing a maximum uptake of 582.6 mg g\(^{-1}\) to be determined. The kinetics of adsorption were analysed using five kinetic models, including those with diffusional bases; overall a pseudo-second-order model best described the adsorption
kinetics, indicating that the process experiences chemical control, likely a combination of ion exchange, diffusion from the bulk to the internal structure of the sorbent and, finally, surface complexation of Cd(II) ions on MATC. The high uptake and low equilibration time, of less than 20 min, indicates that this material has potential for heavy metal remediation from water courses.

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