Lyman-break Galaxies at $z \sim 3$ in the Subaru Deep Field: Luminosity Function, Clustering, and [O III] Emission

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Abstract

We combined deep $U$-band and optical/near-infrared imaging, in order to select Lyman Break Galaxies (LBGs) at $z \sim 3$ using $U - V$ and $V - R_c$ colors in the Subaru Deep Field. The resulting sample of 5161 LBGs gives a UV luminosity function (LF) down to $M_{UV} = -18$, with a steep faint-end slope of $\alpha = -1.78 \pm 0.05$. We analyze UV-to-NIR energy distributions (SEDs) from optical photometry and photometry on IR median-stacked images. In the stacks, we find a systematic background depression centered on the LBGs. This results from the difficulty of finding faint galaxies in regions with higher-than-average surface densities of foreground galaxies, so we corrected for this deficit. Best-fit stellar population models for the LBG SEDs indicate stellar masses and star formation rates of log$_{10}(M_*/$M$_\odot) \simeq 10$ and $\simeq 50$ M$_\odot$ yr$^{-1}$ at $z$ = 24, down to log$_{10}(M_*/$M$_\odot) \simeq 8$ and $\simeq 3$ M$_\odot$ yr$^{-1}$ at $z_{AB} = 27$. The faint LBGs show a $\sim$1 mag excess over the stellar continuum in $K$-band. We interpret this excess flux as redshifted [O III]10$\lambda\lambda$4959,5007 lines. The observed excesses imply equivalent widths that increase with decreasing mass, reaching EW([O III])4959, 5007 + H/β $\gtrsim$ 1500 Å (rest-frame). Such strong [O III] emission is seen only in a miniscule fraction of local emission-line galaxies, but is probably universal in the faint galaxies that reionized the universe. Our halo occupation distribution analysis of the angular correlation function gives a halo mass of log$_{10}(M_*/h^{-1}$M$_\odot) = 11.29 \pm 0.12$ for the full sample of LBGs, and log$_{10}(M_*/h^{-1}$M$_\odot) = 11.49 \pm 0.11$ for the brightest half of the sample.

Key words: cosmology; observations – galaxies: evolution – galaxies: high-redshift – galaxies: luminosity function, mass function – galaxies: star formation – large-scale structure of universe

1. Introduction

Lyman Break Galaxies (LBGs) are selected by the strong and sharp blueward drop in their rest-frame UV continuum, produced by the absorption of photons with energies exceeding the intrinsic Lyman limit (rest-frame 912 Å) at $z \simeq 5.5$, or the Ly$\alpha$ forest of the intergalactic medium at $z \gtrsim 5.5$. The detection of a Lyman break requires that galaxies are actively star-forming, such that their stars produce a strong blue/UV continuum. They therefore tend to have prominent young stellar populations with modest dust extinction. The Lyman break can be defined by optical imaging in only three bands (e.g., Guhathakurta et al. 1990; Steidel et al. 1996). Thus, optical LBG selection has yielded the largest samples of galaxies in the early universe (Steidel et al. 1999, 2003; Shapley et al. 2001; Capak et al. 2004; Dickinson et al. 2004; Giavalisco et al. 2004; Ouchi et al. 2004a; Sawicki & Thompson 2006; Yoshida et al. 2006; Bouwens et al. 2007, 2008, 2010a, 2010b; Iwata et al. 2007; Ly et al. 2009; McLure et al. 2009; Castellano et al. 2010; Fontana et al. 2010; Hathi et al. 2010; Basu-Zych et al. 2011; Bielby et al. 2011; Haberzettl et al. 2012; Bian et al. 2013; Tilvi et al. 2013).

Much observational attention has been focused on the cosmic evolution of the LBG luminosity function (LF) between redshifts of 1.5 and 9 (e.g., Henry et al. 2007, 2008, 2009; McLure et al. 2010; Wilkins et al. 2010; Bouwens et al. 2011a, 2011b). High-redshift LBGs are relatively rare compared to the much larger surface density of foreground objects. Thus, not only must large fields be observed, but it is also useful to have more than one field to overcome the uncertainties imposed by cosmic variance. Examples of such investigations include the European Southern Observatory $U$- and $B$-dropout survey (Hildebrandt et al. 2007), and the Very Large Telescope VIMOS LBG survey (Bielby et al. 2011). These surveys both combine at least five fields to cover nearly 2 deg$^2$. While large sky areas must be surveyed, there is a conflicting requirement for extremely deep photometry to study the fainter side of the LBG LF, which is of great cosmological interest (e.g., Reddy & Steidel 2009; Alavi et al. 2014). Learning more about the old stellar population present in these galaxies requires deep multi-band infrared imaging over large areas, which is even more observationally challenging than the optical imaging.

In this paper, we use the unique imaging of the Subaru Deep Field (SDF) [13$^h$24$^m$, +27$^\circ$29$'$ (J2000)] to study LBGs in a moderately wide field that is also very deep. This provides an LBG sample with good statistics across the entire LF. Combined with our deep complete multiwavelength photometry, we can then determine additional LBG properties, such as stellar mass and star formation rate (SFR), and directly compare the $U$-dropout selection method with other search methods for high-redshift galaxies. Specifically, measurements of the stellar continuum of $z \sim 3$ galaxies at infrared wavelengths allow for a robust determination of stellar mass by constraining their spectral energy distributions (SEDs). Furthermore, optical nebular emission lines are shifted into the IR at these high redshifts; this gaseous emission can significantly boost broadband flux over the expected stellar...
continuum, changing the appearance of the SEDs (e.g., Yabe et al. 2009; Atek et al. 2011; Shim et al. 2011; González et al. 2012; Oesch et al. 2013; Pirzkal et al. 2013; Stark et al. 2013; de Barros et al. 2014; Ly et al. 2016). For example, this effect has been observed for a handful of individual $z \sim 7$ and $z \sim 8$ galaxies as an excess in the Spitzer/IRAC [3.6] and [4.5] $\mu$m bands, respectively, and is attributed to contamination from redshifted [O III]$\lambda\lambda$4959,5007 and H$\beta$ emission (Labbé et al. 2013; Smit et al. 2014). Here, we employ stacking techniques to investigate average UV-to-IR SEDs of the $z \sim 3$ LBGs down to very faint magnitudes.

A further motivation for our SDF study is the importance of measuring the spatial clustering of a deep LBG sample in a large connected field, which cannot be replaced by separate individual smaller fields (e.g., Giavalisco et al. 1998; Giavalisco & Dickinson 2001; Daddi et al. 2003; Foucaud et al. 2003; Ouchi et al. 2004b, 2005; Adelberger et al. 2005; Kashikawa et al. 2006; Lee et al. 2006; Hildebrandt et al. 2007; Ichikawa et al. 2007; Quadri et al. 2007; Yoshida et al. 2008; Furusawa et al. 2011; Bian et al. 2013; Bielby et al. 2013). Clustering analysis of LBGs is an effective probe of the relationship between dark matter halos and the galaxies they host. In the standard theoretical framework of galaxy evolution, the large-scale distribution of (visible) galaxies is determined by the distribution of underlying (invisible) dark halos. Increasing halo mass is expected to be well-correlated with stronger spatial clustering (e.g., Mo & White 1996; Nagamine et al. 2010; Lacey et al. 2011). Such an effect has been observed in LBGs. The clustering strength of LBGs increases with UV luminosity (e.g., Giavalisco & Dickinson 2001; Ouchi et al. 2004b; Adelberger et al. 2005; Lee et al. 2006; Hildebrandt et al. 2007). Because dust-corrected UV luminosity is directly related to SFR, this may imply that the star formation activity of LBGs is controlled by the mass of dark halos that host them.

The very deep multi-wavelength photometry that has been assembled in the large area of the SDF now allows us to make a detailed survey of LBGs and their properties and clustering. To construct a large sample of LBGs at $z \sim 3$, we obtained $U$-band imaging of the SDF with the MOSAIC camera on the Mayall 4 m telescope. This was combined with the very deep optical multi-waveband imaging data obtained by the Suprime-Cam along with deep $I, H$, and $K$ data taken with the wide-field near-infrared camera (WFCAM) on the United Kingdom Infrared Telescope (UKIRT), $H$-band imaging from the NOAO Extremely Wide-Field Infrared Imager (NEWFIRM), and Spitzer Space Telescope Infrared Array Camera (IRAC) maps taken at 3.6, 4.5, 5.8, and 8.0 $\mu$m.

The organization of this paper is as follows. In Section 2, an account of the observations and the data is presented. The selection of the large sample of $z \sim 3$ LBGs is described in Section 3. We also describe simulations to assess the redshift distribution function and the contamination of the sample by interlopers. The LF of the LBGs is presented in Section 4. We infer global physical properties of the LBGs from their stacked UV-to-IR SEDs in Section 5. Here, we also report a detection of [O III]$\lambda\lambda$4959,5007+H$\beta$ emission-line contamination in the stacked $K$-band data, which implies very high equivalent widths in faint, low-mass LBGs. The clustering analysis is presented in Section 6. Our summary and conclusions are given in Section 7.

### Table 1

| Band   | $\lambda_{cont}$ (Å) | $\Delta \lambda$ (Å) | Seeing FWHM (arcsec) | SDF Coverage (%) |
|--------|----------------------|----------------------|----------------------|------------------|
| $U$    | 3630                 | 750                  | 27.19                | 1.49             | 100          |
| $B$    | 4440                 | 690                  | 28.45                | 0.93             | 100          |
| $V$    | 5460                 | 890                  | 27.74                | 0.940            | 100          |
| $R_c$  | 6520                 | 1100                 | 27.80                | 0.97             | 100          |
| $i'$   | 7660                 | 1420                 | 27.43                | 0.98             | 100          |
| $z'$   | 9020                 | 960                  | 26.62                | 0.98             | 100          |
| $J$    | 12560                | 1600                 | 24.75                | 1.10             | 82           |
| $H$(WFCAM) | 16510               | 2900                 | 24.05                | 1.10             | 67           |
| $H$(NEWFIRM) | 16190              | 3000                 | 24.20                | 0.90             | 95           |
| $K$    | 22360                | 3400                 | 24.15                | 1.10             | 82           |
| [3.6]  | 35500                | 7500                 | 24.29                | 1.92             | 81           |
| [4.5]  | 44930                | 10150                | 23.97                | 1.79             | 75           |
| [5.8]  | 57310                | 14250                | 22.86                | 2.00             | 81           |
| [8.0]  | 78720                | 29050                | 22.89                | 2.23             | 75           |

Notes:
- $^a$ Centroid wavelength for the filters in Å.
- $^b$ Filter bandwidths in Å, not counting atmospheric transmission.
- $^c$ Limiting magnitudes measured in 2″-diameter apertures across all portions of the image utilized in the study (across regions of non-uniform depth).
- $^d$ Coverage of the SDF in each image that was utilized for this study. Full coverage corresponds to 876 arcmin².

Throughout this paper, we use the AB magnitude system (Oke & Gunn 1983). We adopt a flat universe cosmology with $\Omega_m = 0.3$, $\Omega_{\Lambda} = 0.7$, and $H_0 = 100$ km s$^{-1}$ Mpc$^{-1}$, where $h = 0.7$, $\sigma_8 = 0.9$, and baryonic density $\Omega_b = 0.04$. However, all dark halo mass parameters presented in the clustering analysis are expressed in units of $h^{-1}$ Mpc to facilitate comparison with previous results.

### 2. Data

#### 2.1. Imaging Data

The SDF has a set of very wide and deep multi-waveband optical imaging data from the Subaru Deep Survey project. These data cover one Subaru/Suprime-Cam field (Miyazaki et al. 2002) $34' \times 27'$ in size, with $0''$202 pixels, in five standard broad-band filters, $B, V, R_c, i'$, and $z'$.

The observations, data processing, and the source detections are described in Kashikawa et al. (2004). Basic parameters are summarized in Table 1. The $3\sigma$ limiting magnitudes of the Suprime-Cam imaging, measured in 2″-diameter apertures, are 28.45, 27.74, 27.80, 27.43, 26.62 in $B, V, R, i'$, and $z'$, respectively. The final co-added image has an effective area of 876 arcmin², with a seeing FWHM of $0''98$ in each band. The wide FOV enables us to probe large comoving volumes exceeding $10^6$ Mpc³ for our LBG sample at $(z) \sim 3$. The absolute error of astrometry was found to be $0''21-0''27$.

Below, we describe the $U$-band, NIR ($J, H, K$-band), and mid-IR data of the SDF utilized for this study. The photometric sensitivity, seeing, and image scales and sizes for these data are summarized in Table 1.

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6 The SDF images and catalogs are available at [http://soaps.nao.ac.jp/](http://soaps.nao.ac.jp/).
2.1.1. U-band Imaging

U-band data were obtained from the Kitt Peak National Observatory Mayall 4m telescope using the MOSAIC-I Imager (Muller et al. 1998) with a FoV of 36′, on 2007 April 18/19, in the SDF, under NOAO proposal Proposal ID 2007A-0589 (Ly et al. 2007b). Details of the observations and data reduction are described in Ly et al. (2011b) (hereafter, L11).

The imaging was centered on the single FoV of the Suprime Cam. Observing conditions were dark (new moon) with minimal cloud coverage. A series of 25-minute exposures was obtained to accumulate 47.4 ks of integration. A standard dithering pattern was followed to provide uniform imaging across the CCD gaps of about 10′.

The MSCRED IRAF (version 2.12.2) package was used to reduce the data and produced final mosaic images with a pixel scale of 0′′.258 and an average-weighted seeing of 1′′.49 FWHM. The reduction steps closely followed the procedures outlined for the reduction of the NOAO Deep Field Survey MOSAIC data.

While several standard star fields (Landolt 1983) were observed, Landolt’s U-band filter differs significantly from the MOSAIC/U, which makes it difficult to photometrically calibrate the data. Instead, 102 Sloan Digital Sky Survey (SDSS) stars distributed uniformly across the eight MOSaic-1 CCDs with u′ ≤ 21 mag were used. This approach requires a transformation between SDSS u′ and MOSAIC/U, which was obtained by convolving the spectrum of 175 Gunn–Styker stars (Gunn & Stryker 1983) with the total system throughput at these wavebands. The 3σ limiting U-magnitude is 27.19 in a 2′-diameter aperture, and 26.52 in a 3′-diameter aperture.

2.1.2. Near-infrared Imaging

J, H, and K-band imaging of the SDF was taken with UKIRT/WFCAM (Casali et al. 2007) during the period from 2005 to 2010. The initial data set in J and K, which cover a part of the SDF, and full data in K are described in Hayashi et al. (2007) and L11. Because WFCAM is composed of four detectors with 13′′.65 × 13′′.65 FoVs with a gap of 12′′/3, four pointings are required to continuously cover the SDF. With the final data set, the J and K-band data cover the whole area of the SDF, with varying image depths across the field (see below). The H data are available for only 67% of the SDF, as we could not complete the fourth pointing in this band. The integration times vary depending on the pointings in each band; 1.1–10 hr in J, 1.0–5.0 hr in H, and 0.4–5.0 hr in K. Data reduction was made in the standard manner for NIR imaging data, using our own IRAF-based pipeline. Spurious objects due to crosstalk of bright objects were carefully excluded. Next, all the images were smoothed with a Gaussian kernel so that their PSF sizes have 1′′.1 FWHM. Astrometry and flux calibration to derive the magnitude zero point were performed by using the 2MASS point-source catalog (Skrutskie et al. 2006). The mosaic of the images taken in different pointings result in non-uniformity in the integration times over the SDF. Nearly half (49%) of the SDF is uniformly deep in all three bands, with 5σ limiting magnitudes in a 2′′ diameter aperture of 24.2 (J), 23.5 (H), and 23.6 (K). On the other hand, 33% of the SDF has moderately deep J and K data with limiting mags of 23.2 (J) and 23.4 (K). The remaining 18% of the SDF is covered in all bands, but only shallow data are available with depths of 22.8 (J), 22.5 (H), and 22.0 (K).

We also utilize more recently acquired H-band data with NEWFIRM. The NEWFIRM imaging data were acquired on 2012 March 06/07 and 2013 March 27/30 with photometric observing conditions at KPNO, clear skies, and 0′′.9 seeing. These conditions were significantly better than in 2008, when the seeing was 1′′.3 with transparency varying by as much as ∼2 mag. The improved observing conditions yielded a mosaicked image that is ∼1.8 mag deeper than our previous H-band observations described in L11. These NEWFIRM data were reduced following the steps outlined in Ly et al. (2011a) with the IRAF irfextm package.

2.1.3. Mid-infrared Imaging

The SDF has been imaged in the mid-infrared with Spitzer/IRAC Channels 1–4, at 3.6, 4.5, 5.8, and 8.0 μm (Fazio et al. 2004). The data used for this project were super mosaics obtained from the Spitzer Heritage Archive.7 Contributing observations to these mosaics are described in Ota et al. (2010); Jiang et al. (2013), and L11. These mosaics cover roughly 80% of the SDF in [3.6] and [5.8], and 75% in [4.5] and [8.0]. The median PSF FWHMs are 1′′.92, 1′′.79, 2′′.00, and 2′′.23 in the [3.6], [4.5], [5.8], and [8.0] mosaics, respectively. The 3σ limiting magnitudes, estimated by performing photometry in 2″ apertures placed randomly throughout the mosaics, are 24.29 ([3.6]), 23.97 ([4.5]), 22.86 ([5.8]), and 22.89 ([8.0]). Additional information on the IRAC instrument properties can be found in the IRAC Instrument Handbook.8

2.2. Photometric Catalogs

Object detection and photometry were performed using SExtractor (version 2.3; Bertin & Arnouts 1996). We masked out regions of low S/N at the edges of the image, near bright stellar halos, and saturated CCD blooming, as well as bad pixels of abnormally high or low count spikes. We first detected objects in the (extremely deep) R′-band image. We considered an object detected when if had more than five contiguous pixels detected at greater than the 2 × rms threshold.

For each detected object, photometry was performed in the other waveband images at exactly the same positions by running SExtractor in dual-image mode. We adopted Kron aperture magnitudes (MAG_AUTO) in SEtractor for total magnitudes, and used magnitudes within a 2″ diameter aperture to derive colors.9 We applied a differential aperture correction of −0.2 mag to the U magnitudes to compensate for the larger PSF size in the U-band image. The value −0.2 was determined so that the difference between the aperture magnitudes and the total magnitudes of the U band became equal to those of the other bands for LBG candidates.

The magnitudes of objects were corrected for a small amount of foreground Galactic extinction using the dust map of Schlegel et al. (1998). The value of E(B − V) = 0.017

7 http://irsa.ipac.caltech.edu/applications/Spitzer/SHA/
8 http://irsa.ipac.caltech.edu/data/SPITZER/docs/irac/iracinstrumenthandbook/
9 We also measured magnitudes within a larger aperture of 3″ diameter, as the PSF FWHM of the final images is somewhat larger in the U-band than in the BVRI′/yc′ bands. However, because over 90% of the LBG candidates selected with 2″ aperture magnitudes overlap those selected with 3″ aperture magnitudes, we adopted 2″ aperture magnitudes in order to obtain the colors of faint objects with better S/N ratios.
In Figure 1, we show the distribution of detected objects in the $U-V$ versus $V-R_c$ diagram, as well as predicted positions of high-redshift galaxies (described below) and foreground objects (lower-redshift galaxies and Galactic stars). We assigned the 1σ limiting-magnitude for objects with $U$ and/or $V$ magnitudes fainter than this level.

We set the selection criteria for LBGs at $z \sim 3$ as:

\begin{align*}
23.0 & \leq R_c \leq 27.8, \\
U - V & \geq 0.12, \\
U - V & \geq 4.1 \times (V - R_c) + 1.8, \\
and \quad V - R_c & \leq 0.41.
\end{align*}

The selection boundaries in the $U-V$ versus $V-R_c$ diagram defined by these color criteria are outlined with the thick black line in Figure 1. The small dots represent all objects we measured in SDF brighter than $R_c = 27.8$. Gray symbols represent galaxies detected in the $U$ band; the more numerous (70% of the sample) blue symbols represent LBGs with upper limits in the $U$ band, meaning that their true locations in the diagram could be higher than what is shown.

To include extremely faint LBGs with low photometric SNRs, we accepted galaxies with formal $U-V$ colors down to 0.12 mag. This is bluer than allowed by some previous searches for “U-dropouts,” but it turned out that this made hardly any difference. If instead we had set the $U-V$ cut at $\geq 0.50$ mag, we would only have lost 48 LBG candidates—less than 1% of our final sample. This would not have significantly changed any of our results.

In general, our color selection is deliberately conservative. We have excluded relatively red LBGs from our sample because we wanted to minimize the possible contamination from foreground interlopers. We have thus aimed to construct a $z=3$ LBG sample of high purity. Although its completeness may be lower than some previous studies, we are able to estimate and correct for this effect (described in Section 3.3). We also excluded candidates brighter than $R_c = 23.0$ because, at that high brightness level, extremely rare, very luminous LBGs would likely be overwhelmed by spurious contaminants.

The data were compared with the predicted colors of model galaxies that are expected to span the range of properties found in LBGs, shown as the red circles. These models were produced using the stellar synthesis code of Bruzual & Charlot (2003) (hereafter BC03), assuming a Salpeter IMF. We considered both constant and exponentially decaying SFR histories. In our modeling of the stellar populations of LBGs, we have considered three metallicities, $Z = 0.004, 0.008$ and 0.02 (solar), and ages of 0.01, 0.1, 0.5, and 1 Gyr. We assumed reddenings of $E(B-V) = 0.0, 0.1, 0.2, 0.3,$ and 0.4, and the Calzetti et al. (2000) attenuation curve. Although we have no particular reason to believe that this law is more applicable to LBGs than other possibilities, we adopt it to facilitate comparison with many previous studies that also assume the Calzetti et al. (2000) curve. The absorption due to the intergalactic medium was applied following the prescription by Madau (1995). The colors were calculated by convolving the constructed model spectra with the response functions of the Suprime-Cam and MOSAIC broadband filters. These models were computed at redshift intervals of $\Delta z = 0.1$. These values reproduce the average rest-frame ultraviolet-optical SED of LBGs observed at $z \sim 3$ (e.g., Papovich et al. 2001; Shapley et al. 2001; Ly et al. 2011b).

Figure 1. $U-V$ vs. $V-R_c$ diagram for the selected LBGs, shown as small dots. Cyan indicates a lower limit for $U$ (and thus $U-V$), whereas gray indicates an object detected at $>U-$ in $U$. The yellow stars mark 175 Gunn & Stryker (1983) stars. The thick black lines indicate the boundary that we adopt for the selection of $z \sim 3$ LBGs. Solid lines show example tracks for model spectra of young star-forming galaxies. The redshift range of the models is from $z = 2-4$, with the circles on the track marking intervals of $\Delta z = 0.1$ (increasing upward in the diagram). The large squares on each track mark redshifts of $z = 2.9$ and $z = 3.5$. The red tracks show colors of model spectra of solely the stellar continuum, with reddening of $E(B-V) = 0.3, 0.1, 0$ and 0, going from right to left. The three right-most tracks are averages of galaxy templates between ages $10^7-10^{8.5}$ years, all with solar metallicity. The fourth red track from the right shows a very blue stellar continuum—an average of ages $10^7-10^{8.5}$ years and metallicity of 1/5 solar. The blue track (left-most curve) shows this bluest continuum model with the addition of Ly$\alpha$ emission, $\% = 20 \%$, boosting flux in the $V$-band. We thus believe that our criteria can effectively select faint galaxies with strong nebular emission. In our fitting to average SEDs of LBGs described below, we confirm that these stellar population parameters cover the same range as the actual galaxies, at least on average.
The red lines in Figure 1 show some of our BC03 stellar synthesis model tracks. Regardless of the stellar population, our selection box is sensitive to LBGs having redshifts of \( z \approx 2.9–3.5 \) (the squares on the model tracks bracket this range). The yellow stars show observed colors of Gunn & Stryker (1983) stars. For a given \( V - R_c \) color, the stars are always bluer in \( U - V \), because they do not have so steep a “\( U \)-drop” as our LBGs. This is not the case for the \( U_gGR \) selection criterion, which is affected by contamination from main-sequence stars L11. The total number of LBGs selected is 5161, with a raw detected surface density of \( \approx6 \) arcmin\(^{-2}\).

A small fraction of our LBG candidates (roughly 15%) have clear \( U \) dropouts (\( U - V \approx 1 \)) while showing extremely blue \( V - R \) colors (of \(-0.3 \) to \(-0.4 \)). Their \( V - R \) colors appear to be 0.1–0.2 mag bluer than our most extreme young starburst model. Closer examination reveals that these blue objects are entirely confined to our faintest LBG candidates (\( R \gtrsim 27 \)), of which they constitute the majority. They are, by definition, required to have solid detections in the \( V \) band, but with otherwise quite noisy photometry. Thus, given their large photometric uncertainties, their true \( V - R \) colors are probably somewhat redder than shown in the diagram, in many cases. As discussed below, we have modeled these photometric uncertainties and find that our selection of LBGs fainter than \( R = 27.0 \) is, indeed, extremely incomplete. However, even at these faint magnitudes, we subsequently find that the contamination fraction of non-LBG interlopers must be small. This is demonstrated by the extremely strong \( K \)-band excess that the stack of our 1294 faintest LBG candidates show, attributable to [O III]5007 emission at \( z \approx 3 \), discussed in Section 5.

Beyond photometry errors, there is an additional factor that may cause the extremely blue \( V - R \) colors in our faintest LBG candidates. As discussed in Section 5.3.1, the strong nebular emission we find in all faint LBGs is also seen in substantial \( \text{Ly}\alpha \) emission, which can be strong enough to increase the observed broadband \( V \) flux. The blue track (left-most curve) shows the model of the youngest stellar population with the addition of \( \text{Ly}\alpha \) emission, \( W_0 = 20 \) Å. This \( \text{Ly}\alpha \)-enhanced track matches the colors of our faintest, bluest LBG candidates.

### 3.2. Number Counts

Table 2 gives the distribution of \( R_c \)-band magnitudes along with surface density counts of our 5161 LBGs. Our sample includes \(~2000\) LBGs fainter than \( R = 27.0 \). This gives us a significantly better statistical measure of the faint end of the LBG LF than previous studies, which covered smaller areas or were less sensitive.

The surface density counts of our LBG candidates are consistent with previous studies, except that we have a lower surface density of the brightest LBGs in the SDF. Given the low surface density of such rare luminous galaxies, this apparent discrepancy could be the result of cosmic variance. Another possibility is that these previous surveys might have suffered some contamination from interlopers at the bright end (Ly et al. 2011b).

### 3.3. Redshift Distribution Function

The redshift distribution function of the LBG sample and its completeness were estimated as a function of magnitude through Monte Carlo simulation. We generated artificial LBGs over an apparent magnitude range of \( 23.0 \leq z' \leq 27.5 \), in intervals of \( \Delta m = 0.5 \) and over a redshift range of \( 2 \leq z \leq 4 \), in intervals of \( \Delta z = 0.1 \). Model spectra of the artificial LBGs are constructed using the BC03 stellar population synthesis code, as described above.

The median size of our LBG candidates is FWHM \( \approx1''1 \). Their unresolved or marginally resolved morphology is consistent with previous expectations that the intrinsic half-light diameters of LBGs at \( z \approx 3 \) should be about 2 kpc, or only a few tenths of an arcsecond (Shibuya et al. 2015). There is a significant tail of resolved LBGs—about 10% of them have FWHM \( >2'' \). We assumed that the shape of LBGs is Gaussian. We assigned apparent sizes to the artificial LBGs in our Monte Carlo simulation matching the size distribution of observed LBG candidates measured by SExtractor.

The artificial LBGs were then distributed randomly on the original images after adding Poisson noise appropriate to their magnitudes, and object detection and photometry were performed in the same manner as done for real objects. We generated 30,000 artificial galaxies on the image, and repeated this five times, to obtain statistically accurate values of completeness. In the simulations, the completeness for a given apparent magnitude, redshift, and \( E(B - V) \) value is defined as the ratio in number of the simulated LBGs that are detected and also satisfy the selection criteria to all the simulated objects with the given magnitude, redshift, and \( E(B - V) \) value. We calculated the completeness of the LBG sample by taking a weighted average of the completeness for each of the five \( E(B - V) \) values. The weight is taken using the \( E(B - V) \) distribution function of \( z \approx 4 \) LBGs derived by Ouchi et al. (2004a) (the open histogram in the bottom panel of their Figure 20), which was corrected for incompleteness due to selection biases.

This Monte Carlo simulation ignores the possible systematic positive correlation of \( E(B - V) \) with galaxy luminosity, which is seen in observations by Labbé et al. (2007), Bouwens et al. (2009), and Sawicki (2012). Our simple approach is the same as used by Yoshida et al. (2006), Bian et al. (2013), and also, judging from the descriptions they give, by Reddy & Steidel (2009) and Hathi et al. (2010). We and other groups have not included a correlation between \( E(B - V) \) and
magnitude in our simulations, mainly because determining the true intrinsic correlation is difficult, given the selection effects operating, and any correlation has such a large cosmic scatter that it does not describe many LBGs. The effects of different reddening assumptions have been considered. Reddy et al. (2008) found that their “results are also insensitive to small variations in the assumed $E(B-V)$ distribution as long as the range of $E(B-V)$ chosen reflects that expected for the galaxies.” Similarly, Sawicki & Thompson (2006) concluded that “the dependence of the LF on these assumed dust and age values is negligibly small at $z \sim 4$ and $3$ but becomes more significant at the lower redshifts.”

As shown in Figure 1, the diagonal color cut we used brings in LBGs of all reddenings at nearly the identical redshift, $z = 2.9$, shown by the red squares. This results in a sharp redshift cut-on for our LBG sample. The high-redshift cut-off is, at least in principle, not so sharp. Theoretically, the bluest galaxies could still fall within the selection box up to a redshift of $z \lesssim 3.7$, whereas the reddest galaxies begin to leave the box at $z > 3.3$. This is a common feature of $U$ dropout selections: toward the flux limits of the surveys, redder galaxies have a somewhat smaller chance of being included. Our simple Monte Carlo simulation selected galaxy reddenings independent of their magnitude. A more sophisticated simulation might have included a tendency for brighter LBGs to be redder, presumably because of higher dust content (Steidel et al. 2003). This could reveal a weak bias in favor of discovering bluer LBGs at lower redshifts. We, along with others using two-color selections, have not included such a correlation into our completeness simulations. To the extent that this correlation is not merely a selection artifact of magnitude-limited surveys, its form is quite uncertain, with a great deal of intrinsic scatter. In any case, the reality, shown in the figures, is that our selection finds very few LBGs—of any type—at $z \gtrsim 3.5$. There is therefore little room for a possible (highly uncertain) color bias to undermine our completeness estimates.

The resulting completeness, $p(m, z)$, is shown in Figure 2. Because we have been careful to make generous allowances for the number of LBGs that could have been missed due to reddening, our total completeness is not extremely high, dropping to 50% at $R_e = 25.0$ and 20% at $R_e = 26.0$. This means that a large number of our fainter LBGs are in a regime where our survey (and nearly all others) is not very complete. The magnitude-weighted redshift distribution function of our LBG sample was derived from $p(m, z)$ by averaging the magnitude-dependent completeness weighted by the number of LBGs in each magnitude bin. The average redshift and its standard deviation are calculated to be $\langle z \rangle = 3.3$ and $\sigma_z = 0.3$.

A small minority (140) of the 5161 LBGs are individually detected ($>3\sigma$) in both of the WFCAM $H$ and $K$ band images (hereafter referred to as our NIR subsample). Of these, slightly over half (77) are also detected in IRAC bands 1 and 2. These are naturally the reddest LBGs in the parent sample and are expected to be the most massive (containing older stellar populations) or dust-obscured. So, although they are not representative of the full LBG population as a whole, they do have enough accurate multi-band photometry over a wide wavelength range to allow us to measure their photometric redshift distribution. In particular, the $H$ and $K$ band photometry spans the Balmer break at these redshifts. We input their optical-to-infrared SEDs into the Easy and Accurate Zphot from Yale (EAZY; Brammer et al. 2008). The resulting distribution of $z_{\text{phot}}$ for the NIR subsample is shown in Figure 3. The NIR subsample has a median redshift $\langle z_{\text{phot}} \rangle_{\text{med}} = 3.03$, with $\sim 90\%$ of the LBG candidates having photometric redshifts in the range $2.5 - 3.5$. Thus, robust photometric redshifts derived for a subset of massive LBGs yield confidence in the effectiveness of our color selection (described above) to select $z \sim 3$ star-forming galaxies. We further discuss properties of the NIR subsample in Section 5.

3.4. Comparison with $U_{\text{drop}} - G$ Dropouts in SDF

The same $UBVR_{\text{i}}/i'z'$ photometry in SDF was previously used by L11 to identify LBGs. That study aimed to duplicate exactly the $U$-dropout method used by Steidel and collaborators, which selects objects with very red $U_e - G$ colors (e.g., Steidel et al. 1999). L11 approximated the $G$ filter with a linear combination of $B$ and $V$ photometry. Because the $G$ band is about 500 Å bluer than the $V$ band used in this paper, their LBG sample starts at $z = 2.5$ rather than our $z = 2.8$. This results in their finding a higher surface density of bright $U$-dropouts than...
we did with our $U-V$ selection. However, when we account for the different selection functions and cosmic volumes surveyed, our resulting LF is very similar to that of $U_G$ dropouts (see Section 4 below). In contrast to our selection down to $R_e = 27.8$, L11 cut their LBG selection at relatively bright $U$-dropouts, having $R \leq 25.5$. They also used a combination of photometric and image size information to exclude stars, which removed about 10% of the LBG candidates at $R < 24$, and a smaller, negligible fraction fainter than that. Overall, from cross-matching our $U-V$ dropout catalog with the $U_G$ dropout catalog in L11, we find only 651 sources in common (13% of our sample and 27% of the L11 sample). This lack of overlap is due to the effects mentioned above—primarily the differing color selections. Our sample occupies a bluer, fainter locus on the $U-V$ versus $V-R_e$ diagram than the $U_G$ dropouts from L11. For comparison, we included the L11 sample in our analysis of average UV-to-IR SEDs and inferred physical properties discussed in Section 5.

4. LBG Luminosity Function in the SDF

The LF for the LBG sample at $z \sim 3$ was derived in the same manner as in Steidel et al. (1999) and Yoshida et al. (2006), using the completeness estimates described in Section 3.3. To estimate contamination, we took the fraction of low-redshift interlopers in the LBG sample from the Monte Carlo simulation performed in Yoshida et al. (2008). With an adopted boundary redshift of $z_0 = 2.9$ between interlopers and LBGs, they find the fraction of low-redshift interlopers to be, at most, 6% at any magnitude.

The effective volume is defined as:

$$V_{\text{eff}}(m) = \int_{z_0}^{\infty} p(m, z) \frac{dV(z)}{dz},$$

where $p(m, z)$ is the completeness function described in Section 3.3. We estimated this for our 876 arcmin$^2$ field using:

$$\frac{dV(z)}{dz} = \left( \frac{D_L}{1+z} \right)^2 \times 876 \times \left( \frac{\pi}{10800} \right)^2,$$

where $D_L$ is the luminosity distance. The quantity $dzdV/dz$ is the comoving volume per arcmin$^2$ at redshift $z$ (see Steidel et al. (1999) for discussion). The effective volumes for each magnitude range and the number of observed LBGs are given in Table 2. The absolute magnitudes of the LBGs were determined assuming a flat UV continuum (i.e., $\lambda f_\lambda$ [erg s$^{-1}$ cm$^{-2}$ Å$^{-1}$] is constant), such that the apparent UV magnitudes of the LBGs, $m_{\text{UV}}$, are simply their $R_e$-band magnitudes (corresponding to rest-frame $\lambda \sim 1600$ Å). Then:

$$M_{\text{UV}} = m_{\text{UV}} - 5 \log_{10} \left( \frac{D_L}{10 \text{ pc}} \right) + 2.5 \log_{10}(1+z),$$

with an assumed redshift of $z = 3$. Note that the $K$-correction term is excluded, as it is nearly zero (Sawicki & Thompson 2006).

Figure 4 shows our LBG LF in comparison to those from other studies of galaxies at $z = 3$ (Steidel et al. 1999; Sawicki & Thompson 2006; Yoshida et al. 2008; Reddy & Steidel 2009; Hathi et al. 2010; Bian et al. 2013). More determinations of the LBG LF have been made by Rafelski et al. (2009) and van der Burg et al. (2010). Our LF mostly agrees well with those in the literature, particularly when one considers the different sample selections. The LFs from Sawicki & Thompson (2006) and Hathi et al. (2010) appear to be significantly lower at the faint end, perhaps due to insufficient corrections for incompleteness.

Interestingly, the SDF $z \sim 3$ LBG LF we observe shows only a very gradual downward curvature. Therefore, there is not a very clearly defined “knee” at which it turns over, as in a Schechter function. In fact, a double power law would likely give a better fit to the data, with a relatively small flattening of slope at low luminosities. Nonetheless, for comparison with previous studies, we fit our LF with the standard Schechter function, described by:

$$\phi(M_{\text{UV}})dM_{\text{UV}} = \phi^* \left( \frac{\ln 10}{2.5} \right) (10^{-0.4(M_{\text{UV}} - M^*_{\text{UV}})})^{\alpha+1} \times \exp \left( -10^{-0.4(M_{\text{UV}} - M^*_{\text{UV}})} \right) dM_{\text{UV}},$$

where $M^*_{\text{UV}}$ is the characteristic absolute magnitude, $\phi^*$ is the normalization, and $\alpha$ is the faint-end slope. The best-fitting Schechter function parameters (along with those derived for other LBG studies) are given in Table 3. Indeed, we derive a steep faint-end slope of $\alpha = -1.78 \pm 0.05$ indicative of the high abundance of faint, low-mass systems in the universe. We note that Bian et al. (2013) derives an even steeper faint-end slope of $\alpha = -1.94 \pm 0.10$; however, their sample is much shallower than ours, only reaching $M_{\text{UV}} = -20.8$.

5. Physical Properties of LBGs

We inferred physical properties of the LBG sample from their UV-to-IR SEDs. As described in Section 3.3, a subset of 140 LBGs are detected in $H$ and $K$ bands with about half of these galaxies detected in IRAC bands 1 and 2 as well. However, the majority of our LBGs have relatively blue colors and are too faint to be detected in the IR. In order to study our sample as a whole, we obtained average detections of LBGs in the infrared by stacking on their optical positions in the long-wavelength images. The large number of LBGs in our sample...
allows us to probe LBG properties such as stellar mass down to very faint magnitudes.

5.1. LBG Stacking

To stack LBGs in the infrared, we divided our sample into bins of $i'$-magnitude, a proxy of SFR at $z \sim 3$ (probing rest-frame $\sim$1900 Å). Specifically, we stacked our sample of LBGs in bins of $i' = 23.5-24.5, 24.5-25.5, 25.5-26.5$ and $26.5-27.5$. These magnitude bins contain 249, 806, 1256, and 1588 LBGs, respectively. The $\sim$1200 LBGs with $i' > 27.5$ did not yield stacked detections, and are thus excluded from the following analysis. An image of a representative galaxy in each magnitude bin was formed by finding the median of each pixel in stacks of roughly $30'' \times 30''$ cut-outs, centered around the optical position of each LBG in the bin. Here, we use the median of pixels rather than the mean, as the latter is significantly more prone to outliers.

Stacking is performed in the WFCAM $K$-band and all four IRAC mosaics (3.6, 4.5, 5.8, and 8.0). Stacked fluxes were obtained from aperture photometry on the stacked images. We applied aperture corrections that were determined for the WFCAM/NEWFIRM images of the SDF by identifying bright/isolated point sources and computing the median curve of growth. For the IRAC mosaics, we used the aperture corrections given in the IRAC Instrument Handbook. As a check, we calculated our own aperture corrections and found that they are within 0.1 mag of those quoted in the handbook. Examples of stacked images of our LBGs in the $K$-band and IRAC 3.6 μm mosaics are shown in Figure 5.

For each image, we computed the statistical significance of stacked flux as follows. First, we generated a set of $N$ random image coordinates (in the same regions used for stacking), formed a median-stacked image for these $N$ random coordinates, and found the aperture flux (with the same aperture size used to measure our LBG stacked flux). We then repeated this process for 1000 iterations to form a distribution of aperture flux from stacks of random image positions. The width of this distribution (which is Gaussian) gives the 1σ flux level corresponding to aperture photometry for stacks of $N$ coordinates on a given image of the SDF. Thus, we derived curves of 1σ flux versus number of coordinates in a stack $N$ for each image. As expected, we find that every curve follows a $1/\sqrt{N}$ law. For each band, the 3σ limiting-magnitudes from stacking $N = 1000$ sources, after aperture correction, are: $J = 27.44, H$ (WFCAM) = 26.86, $K$ (WFCAM) = 26.39, $3.6\mu m$ (IRAC) = 25.07, $4.5\mu m$ (IRAC) = 24.57, $5.8\mu m$ (IRAC) = 24.29, and $8.0\mu m$ (IRAC) = 23.64.

Note. The corrections for a 4''8-diameter aperture are $0.21, -0.22, -0.33$, and $-0.48$ mag in the [3.6], [4.5], [5.8], and [8.0] mosaics, respectively.
bias is due to SExtractor requiring a lower local background level when attempting to stack on fainter objects in the detection catalog. When we encounter perhaps the largest source of uncertainty in this defect and determine an appropriate method to correct for it, we run SExtractor on the new detection image (with all the synthetic galaxies added), with parameters identical to those used for LBG detection, and recovered the coordinates of all detected synthetic objects. According to our hypothesis, these coordinates should be positions with relatively lower background for fainter objects in the detection image. Finally, we stacked on those positions in the IR and obtained a “hole” representing the pure background deficiency (because the synthetic galaxies were added only to the detection image). This effect is shown in Figure 6. Stacking on all fake object input positions (which are just random image coordinates) results in a uniform stack with no hole apparent. As expected, the amplitude (depth) of the hole gets deeper as the fake galaxies added are increased in size.

In summary, we confirm that faint objects in SExtractor detection catalogs are located in regions of lower local background (due to a lack of faint, blended sources) than the brighter sources in the catalog. This effect is also likely present in catalogs generated with other detection algorithms. Thus, in any study utilizing such catalogs for stacking analysis of faint objects, the stacked flux of these objects will be systematically underestimated if this defect is not accounted for. We also note that low-resolution images that are deep enough to begin to

\[ H(\text{NEWFIRM}) = 26.74, \ K = 27.12, \ [3.6] = 26.34, \ [4.5] = 26.35, \ [5.8] = 24.82, \text{ and } [8.0] = 24.85. \]

5.1.1. Faint-stack Defect and Corrections

In the stacks of fainter bins, such as in those displayed in Figure 5, we encounter perhaps the largest source of uncertainty in stacked flux: a depression in the background within the immediate vicinity (\( \lesssim 10'' \)) of the detected source. To understand the cause of this defect and determine an appropriate method to correct for it, we performed the following analysis. First, we used publicly available SDF SExtractor detection catalogs\(^{11}\) and stacked on random source positions listed in the catalog, binning by \(i'\) magnitude (down to total mag of \(i'' = 29\)). The defect remains present in these test stacks of a very heterogeneous sample, so we rule out the defect as being a result of our LBG selection technique. We find that the defect is present in the faint \(i'\)-mag stacks of SDF images in all wavebands, including the publicly available \(BVRi'z'\) images. The deficit gets more severe with fainter source magnitude, and is perhaps most significant in the IRAC [3.6] and [4.5] bands.

From this test, we posit that the defect is caused by background counts around faint sources in the detection catalogs being systematically lower than the background counts around brighter sources. In other words, faint objects tend to enter these catalogs when they are found in regions of the sky with relatively low surface density of faint, blended objects (i.e., low confusion). This bias is due to SExtractor requiring a lower local background level (higher S/N) in order to include a faint source as a detection. To test this hypothesis, we performed a test similar to the calculation of the completeness of our sample. We created 50,000 fake galaxies (Gaussian-shaped) with chosen total magnitude and size, and added them to random positions in the Suprime-Cam \(R_c\)-band image (the detection image), cataloging their random positions. Next, we ran SExtractor on the new detection image (with all the synthetic galaxies added), with parameters identical to those used for LBG detection, and recovered the coordinates of all detected synthetic objects.\(^{12}\) According to our hypothesis, these coordinates should be positions with relatively lower background for fainter objects in the detection image. Finally, we stacked on those positions in the IR and obtained a “hole” representing the pure background deficiency (because the synthetic galaxies were added only to the detection image). This effect is shown in Figure 6.

\(^{11}\) http://soaps.nao.ac.jp/SDF/v1/index.html

\(^{12}\) The recovery rate is roughly 60\%, down to 50\% for synthetic objects with \(R_c = 25\) and \(R_c = 26\), respectively.
approach the confusion limit are particularly affected by this bias.

This systematic loss of faint galaxies in the near vicinity of other galaxies was already corrected for in our LF calculations in Section 4, using our detailed simulations of incompleteness. However, corrections were still required for our stacked images in order to obtain accurate photometric fluxes.

We performed a simple least-squares fit to each image with a two-component model consisting of a positive Gaussian function for the stacked emission and a negative Lorentzian component for the background depression. We fixed both components to be circularly symmetric with centroids on the center of the image. After the fit was performed, the corrected image was generated by subtracting the negative Lorentzian component off of the original stacked image. An example of this correction procedure is shown in Figure 7 for the IRAC 3.6 µm stack in the \((i') = 26\) bin, showing the raw image, the model, and the corrected image along with corresponding radial profiles. Although the fit is good for all stacked images, this correction is considered the primary source of uncertainty in measuring the stacked flux of faint bins.

5.2. LBG Spectral Energy Distributions

We compute representative LBG SEDs using the median of \(UBVR,i'z'\) photometry and photometry from the median stacks of \(J, H, K, [3.6], [4.5], [5.8]\), and \([8.0]\) images in each \(i'\)-mag bin. Prior to measuring fluxes from stacked images, we implemented corrections to all of the NIR through mid-infrared stacks in the \((i') = 25\) bin and fainter, in order to account for the faint stack background deficiency (described in Section 5.1.1). Error bars on stacked fluxes are calculated from the random stack analysis described above. The reported stacked \(H\)-band fluxes are formed from a weighted mean of the flux from the WFCAM and NEWFIRM stacked images. The average SEDs for our \(U - V\) selected LBGs are plotted in the left panel of Figure 8. For comparison, we additionally performed stacking to form SEDs of the sample of \(U_n - G\) selected LBGs from L11. As explained in Section 3.4, this sample is redder and includes a higher proportion of galaxies on the lower-redshift end of our redshift distribution function. We stacked this galaxy sample in three bins: \(i' = 23-24\), \(24-25\), and \(>25\) (the sample is selected with \(R < 25.5\), yielding sources down to \(i' \approx 26\)). The faint stack defect is only non-negligible in the faintest bin \((i') = 25.5\); in this bin, all reported stacked data were corrected using the method described above. The average SEDs for these \(U_n - G\) dropouts are shown in the right panel of Figure 8. We also form the stacked SED of our massive, NIR-detected subset of 140 LBGs.

Average LBG properties as a function of \(i'\) magnitude are derived using the Fitting and Assessment of Synthetic Templates (FAST) code (Kriek et al. 2009) to fit stellar population synthesis templates to each stacked LBG SED. We use the BC03 stellar population template library, with a Salpeter IMF, and assume the Calzetti et al. (2000) dust extinction curve. We fit an exponentially decaying star formation history of the form \(SFR \sim \exp(-t/\tau)\). The ranges of parameter values for fitting are set to: age \(t = 10^{6}-10^{10}\) years, star formation history \(\tau = 10^{7}-10^{9}\) years (in steps of 0.5 dex), and extinction \(A_V = 0-3\). Metallicity is fixed at solar \(Z = 0.02\). For our LBG sample, we fix the redshift of the fit to \(z = 3.1\), which is the approximate peak of the completeness distribution for each magnitude bin. For the L11 sample, we fix the redshift to the median photometric redshift in each bin. The resulting best-fit age, \(\tau, A_V\), stellar mass \(M_*\), and SFR corresponding to each average LBG are given in Table 4. Uncertainties for these physical quantities are determined by FAST, using Monte Carlo simulations that redistribute the photometric data according to their error bars, and include additional uncertainty based on the uncertainties in the stellar

Figure 7. Example of the procedure to correct faint stacked images for the background deficiency defect, applied here to the IRAC [3.6] \((i') = 26\) stack. The top panels show images, from left to right, of the raw (uncorrected) image, the model (consisting of a positive Gaussian emission and negative Lorentzian), and the corrected image with the negative component subtracted out. The bottom panel displays the radial profiles corresponding to the top images.
continuum models (see the appendix of Kriek et al. 2009 for more information).

The SEDs show a $K$-band excess that is more pronounced for fainter bins. We attribute this excess to contamination from redshifted $[\text{O III}]\lambda\lambda 4959,5007 + \text{H}\beta$ nebular line emission. As such, we perform fits both including and excluding the $K$-band photometry. The best-fit models are shown in Figure 8 with the data; the blue and red curves exclude and include the $K$-band data, respectively. The quoted stellar parameters in Table 4 correspond to the blue curves. Note that these fits only consist of a stellar continuum; we discuss the implications of nebular emission in Section 5.3.

### 5.3. Stellar Properties and Nebular Emission

In general, we find that the properties derived for the LBGs studied here, given in Table 4, are consistent with those derived in other studies of $z \sim 3$ star-forming galaxies. We compare our LBG sample to the “star-forming main sequence” (Speagle et al. 2014, and references therein) and plot their $M_\ast$–SFR correlation in Figure 9. The dashed line in Figure 9 is a linear fit to a sample of massive (average stellar mass of $\pm 5 \times 10^{10} M_\odot$) LBGs at $z \sim 3$ studied in Magdis et al. (2010). Our average LBGs have stellar masses between $10^{7.8}$ and $10^{10.1} M_\odot$, and SFRs between 3 and $51 M_\odot$ yr$^{-1}$. As expected, the stack of the NIR-detected sample is more massive, with $M_\ast \approx 10^{10.5} M_\odot$ and SFR $= 45 M_\odot$ yr$^{-1}$. The $\lambda_\delta$ – $\lambda_\gamma$ dropouts in L11 are found to be slightly more massive for a given $i'$ magnitude (which is also expected based on their redder colors). The average LBG in the faintest bin $\langle i' \rangle = 27$ has a best-fit model SED with low stellar mass $M_\ast \approx 10^{8} M_\odot$, very young age $t \approx 10$ Myr, and high specific star formation rate (sSFR) of $10^{-7.2}$ yr$^{-1}$ or 60 Gyr$^{-1}$, placing it nearly $\sim 1$ dex above the fit to the Magdis et al. (2010) sample. Although the fitting parameters are highly uncertain, the properties are indicative of dwarf galaxies forming stars at a prolific rate. Their presence in large numbers suggests that the “star-forming sequence” in reality contains significant dispersion. The smaller the mass of the galaxy, the more stochastic its star formation episodes are likely to be, and the greater scatter this should produce in a $M_\ast$–SFR correlation. This insight is entirely consistent with what surveys at somewhat lower redshifts have found when
Table 4
Stellar Properties of Average $z \sim 3$ LBGs, Derived from Stellar-continuum Fits to the Stacked SEDs

| $i'_{	ext{drop}}^b$ | $N_{\text{stack}}^b$ | log$_{10}(M_*/M_\odot)$ | SFR (M$_\odot$ yr$^{-1}$) | Age (Myr) | $\tau$ (Myr) | $A_v$ |
|-------------------|---------------------|--------------------------|--------------------------|-----------|------------|-------|
| $U - V$ dropouts  |                     |                          |                          |           |            |       |
| 24.3              | 113–140             | 10.47 ± 0.06             | 45 (+3, −17)             | 398 (+233, −194) | 316        | 0.6   |

$U - V$ dropouts

| 24.2              | 169–217             | 10.09 (+0.16, −0.33)     | 51 (+48, −49)             | 251 (+456, −208) | 1000       | 0.5   |
| 25.1              | 589–724             | 9.58 (+0.00, −0.26)      | 12 (+0, −11)              | 251 (+37, −192) | 316        | 0.2   |
| 26.1              | 878–1078            | 9.02 (+0.07, −0.69)      | 3 (+22, −1)               | 251 (+165, −242) | 316        | 0.0   |
| 26.9              | 1138–1390           | 7.79 (+0.74, −0.10)      | 4 (+12, −3)               | 10 (+253, −6)   | 10         | 0.3   |

$U_b - G$ dropouts (L11)

| 23.8              | 104–130             | 10.22 (+0.12, −0.10)     | 27 (+38, −25)             | 100 (+157, −45) | 31         | 0.4   |
| 24.7              | 668–867             | 10.10 (+0.00, −0.30)     | 13 (+0, −12)              | 251 +0, −188   | 100        | 0.3   |
| 25.3              | 826–1048            | 9.54 (+0.14, −0.44)      | 6 (+139, −6)              | 100 (+175, −90) | 31         | 0.1   |

Notes.

$^a$ Median $i'$ mag in bin.

$^b$ Range in number of objects in each stack. The minimum number of objects are in the WFCAM $H$-band stacks due to its incomplete coverage of the SDF.

Figure 9. Star formation rate vs. stellar mass for the stacked LBGs in this study (black), the NIR-detected subset (individual as red X’s and stacked as the red square), and of the stacks of $U_b - G$ dropouts (blue squares) presented in L11. Also shown is an extrapolation of the best-fit line from Speagle et al. (2014) to massive $z \sim 3$ LBGs selected in Magdis et al. (2010), which we shift by a factor of 1.8 in mass in order to scale from their assumed Chabrier IMF to a Salpeter IMF.

5.3.1. Nebular Emission in High sSFR LBGs

Galaxies at the faint end of the LF, especially at high redshifts, have SEDs showing significant contributions from nebular emission (e.g., Yabe et al. 2009; Atek et al. 2011; Stark et al. 2013; de Barros et al. 2014). Indeed, the observed average LBG SEDs in Figure 8 contain some clear features that are not explained by the best-fit stellar continuum models.

Compared with filters on either side, the $K$-band magnitude is brighter by roughly 0.2, 0.4, and 0.9 mag for the $(i') = 25$, 26, and 27 LBG SEDs, respectively. The most likely explanation is that the stellar continuum in the $K$-band is boosted by a strong contribution from [O III] $\lambda$4959,5007 emission at $z \simeq 3.1$–3.8 (with some contribution from H$\beta$). Assuming this interpretation is correct, we estimate the equivalent width $\text{EW}([\text{O III}] \lambda \lambda 4959, 5007 + \text{H}\beta)$ for each average LBG. Specifically, we calculate the expected stellar continuum at the $K$-band wavelength, $m_{2.2, \text{const.}}$, by convolving the best-fit stellar continuum models with the WFCAM $K$-band response curve. Knowing the $K$-band magnitude $m_K$ and the filter FWHM $\Delta K = 0.34$ $\mu$m, we then calculate the observed equivalent widths as:

$$\text{EW}([\text{O III}] + \text{H}\beta) \simeq (1 - 10^{-0.4(m_K - m_{2.2, \text{const.}})}) \cdot \Delta K. \quad (9)$$

Error bars on the equivalent widths are calculated by re-sampling the $H$, $K$, and [3.6] filter fluxes with random noise added based on their photometric errors. Assuming a redshift of $z = 3.1$, the implied rest-frame equivalent widths of the $(i') = 25$, 26, and 27 stacked LBGs are $\text{EW}_{0}([\text{O III}] + \text{H}\beta) \simeq 247 \pm 105$, 443 $\pm$ 143, and 1743 $\pm$ 360 $\AA$, respectively. The $K$-band excess is also observed in the stacked SEDs for the $U_b - G$ dropouts from L11, implying $\text{EW}_{0}([\text{O III}] + \text{H}\beta) \simeq 79 \pm 86$ and 303 $\pm$ 110 $\AA$ for the $(i') = 24.5$ and 25.5 LBGs, respectively.

In order to facilitate comparison with other samples, we remove the predicted contribution of H$\beta$ by assuming ratios for [O III] $\lambda$4959,5007/H$\beta$. The $[\text{O III}]/\text{H}\beta$ ratios were taken from mass-stacked spectra of galaxies in the WFC3 Infrared Spectroscopic Parallel survey (WISPS) in Henry et al. (2013) and Domínguez et al. (2013). Comparing the mean mass and resulting stacked $[\text{O III}]/\text{H}\beta$ in these studies with the stellar mass of our stacked LBGs, we use ratios of [O III]/H$\beta$ = 3.0, 4.5, and 5.0 for our three faintest bins of LBGs, and [O III]/H$\beta$ = 2.5 and 3.0 for the two faintest bins of the L11 $U_b - G$ dropouts.

Figure 10 shows $\text{EW}_{0}([\text{O III}] \lambda \lambda 4959,5007)$ versus stellar mass for the LBGs studied here, compared with emission-line galaxy (ELG) samples at different redshifts. We find a steep dependence of $\text{EW}_{0}([\text{O III}])$ on stellar mass, which we quantify by fitting a simple power-law with amplitude $C$ and slope $p$:

$$\text{EW}_{0}([\text{O III}] \lambda \lambda 4959,5007) = C(\log_{10}(M_*/M_\odot))^{-p}. \quad (10)$$

they select galaxies by their line emission rather than broadband continuum (Atek et al. 2011, 2014; Ly et al. 2014, 2015).  

Figure 10 shows $\text{EW}_{0}([\text{O III}] \lambda \lambda 4959,5007)$ versus stellar mass for the LBGs studied here, compared with emission-line galaxy (ELG) samples at different redshifts. We find a steep dependence of $\text{EW}_{0}([\text{O III}])$ on stellar mass, which we quantify by fitting a simple power-law with amplitude $C$ and slope $p$:
The least-squares fit, shown as the black dashed line in Figure 10, is performed for both the stacks of $U - V$ dropouts selected in this study and the stacks of $U - G_6$ dropouts selected in L11. The LBGs have a best-fit slope of $p = 10.2 \pm 1.5$. Although highly uncertain, the fit implies that the average $z \sim 3$ LBG with a stellar mass of $M_\ast = 10^9 M_\odot$ has a rest-frame [O III] $\lambda 4959,5007$ equivalent-wavelength of $\approx 340$ Å, while a dwarf LBG with $M_\ast = 10^8 M_\odot$ has EW$_{[O III]} \approx 1130$ Å. To emphasize how extraordinarily strong these [O III] emission lines are in the faint LBGs, we note that this doublet is carrying several percent of the entire luminosity of the galaxy. This makes it one of the most distinctive observable features—after the Lyman break—in the entire galaxy spectrum.

Local analogs to the faint LBGs are the “green pea” galaxies that were identified, in the SDSS, by their distinctive green color originating from strong [O III] $\lambda 4959,5007$ emission (Cardamone et al. 2009). The SDSS green peas have masses in the range $\log_{10}(M_\ast/M_\odot) = 8.5 - 10.5$ and typical sSFRs of $\approx 4$ Gyr$^{-1}$, comparable to those derived for our average LBGs (excluding the faintest bin with extremely high implied sSFR). These local [O III]-emitters are quite rare, with a rough surface density of $\sim 10^{-2}$ arcmin$^{-2}$.

Less-massive ELGs at $z \lesssim 1$ are presented in Ly et al. (2015, 2016). In particular, Ly et al. (2015) presents a sample of metal-poor, [O III] $\lambda 4363$-detected $z \approx 0.8$ galaxy sample from the DEEP2 Galaxy Redshift Survey (Newman et al. 2013). These galaxies have high sSFR near 10 Gyr$^{-1}$ and lie about 1 dex above the typical $M_\ast$-sSFR correlation at $z \approx 0.8$, similar to what is observed for the $(i') = 27$ stacked LBG in this study. This sample, shown on Figure 10 as cyan circles, has a median EW$_{[O III]} \lambda 4959,5007 \approx 400$ Å and extends down to $M_\ast \approx 10^8 M_\odot$. The galaxies at $z = 0.1 - 1$ from Ly et al. (2016), selected by narrow-band emission in the SDF, are shown in Figure 10 as red circles. The filled circles represent galaxies with detectable [O III] $\lambda 4363$ emission ($\approx 36\%$ of their sample), while those without detection of this line are shown as open circles. Taken together, these ELGs have a median EW$_{[O III]} \lambda 4959,5007 \approx 160$ Å.

WISPs has produced larger samples of emission-line galaxies at $z \sim 1 - 2$. The properties of our fainter LBGs overlap with some of the more extreme emission-line galaxies in WISP. For example, Atek et al. (2011) selected [O III] and H$\alpha$ emitters with EW $> 200$ Å (rest-frame). The $(i') = 26$ average LBG in our study (with EW$_{[O III]} \approx 360$ Å) is roughly within the top half of the [O III] EW distribution in Atek et al. (2011), while our faintest average LBG $(i') = 27$ has EW$_{[O III]} \approx 1450$ Å, which is in the top $\approx 15\%$. A larger WISP sample, presented in Atek et al. (2014), shows that our average $(i') = 24, 25,$ and 26 LBGs have sSFRs in the top $\approx 40\%$ of these emission-line galaxies. Our faintest average LBG is near the top 5% of their sSFR distribution.

We also compare our LBGs to extreme emission-line galaxies (EELGs) at higher redshift from van der Wel et al. (2011) and Maseda et al. (2014). The galaxies in these studies were selected to have very large EW$_{[O III]}$, strong enough to produce detectable excess in the $J$ and $H$ bands for their samples at $z \sim 1.7$ and $z \sim 2.2$, respectively. These EELGs have typical masses of $10^{10} - 10^{11} M_\odot$, and high sSFRs ($\approx 10$ Gyr$^{-1}$) for the galaxies in Maseda et al. (2014) that are comparable to the best-fit sSFRs for our average LBGs. The $(i') = 27$ stacked LBG from our sample is within the locus of the van der Wel et al. (2011) EELGs in Figure 10. Interestingly, these galaxies have a space density nearly two orders of magnitude higher than the local green peas.

The enhancement of EW$_{[O III]}$ is not only associated with low-mass dwarf galaxies with extreme starbursts, it also appears to increase at higher redshifts across the board. It has long been suspected that [O III] emission is much stronger at higher redshifts ($z > 3$) than in star-forming galaxies at lower redshifts. This was the conclusion of the first narrow-band imaging search for [O III]-line-emitting galaxies at $z = 3.3$ (Teplitz et al. 1999). Near-infrared spectroscopy further confirmed the unusual strength of [O III] in Lyman break galaxies at $z \sim 3$ (Teplitz et al. 2000), and gravitationally lensed galaxies at these redshifts hinted that [O III] was even stronger in the less-luminous galaxies (Teplitz et al. 2004).

The next step forward came with multi-object spectroscopy, using MOSFIRE on Keck, which showed that strong [O III] emission is common among $z \sim 3 - 4$ LBGs. Schenker et al. (2013) found strong $K$-band emission lines in 20/28 targeted LBGs at $z = 3.0 - 3.8$ (13 of which had prior spectroscopic confirmation, and 15 of which were photometrically selected). These galaxies, which overlap the mass range of our sample, have a median EW$_{[O III]} \sim 280$ Å, with a few reaching $\sim 1000$ Å or higher. More recently, Holden et al. (2016) present $K$-band spectra of 15 spectroscopically confirmed and 9 photometrically selected LBGs at $z = 3.2 - 3.8$. Again, strong [O III] emission is detected in 18/24 LBGs (15/15 and 3/9 for the spectroscopic and photometric samples, respectively), with a median EW$_{[O III]} \approx 180$ Å. As shown by Figure 10, our stacked LBGs are quite consistent with their EW distribution. Combined with our result, these studies suggest that the fraction of [O III]-emitters in the LBG population is substantial at $3 < z < 4$. 

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Also shown in Figure 10 (as black and brown open triangles) are the implied EWs from average SEDs of a sample of $I$-dropout galaxies presented in Smit et al. (2014). These $z \approx 7$ galaxies (with masses of $10^{10} - 10^{11} M_{\odot}$) show a very large excess in the IRAC [3.6] filter, which indicates rest-frame equivalent widths of $EW_{\nu}(\text{[O III]}) + H\beta > 637 \AA$ for the average galaxy in the sample and $EW_{\nu}(\text{[O III]}) + H\beta \approx 1582 \AA$ for a subset of the bluest galaxies. Signatures of such strong [O III] + H\beta contamination are also reported for a handful of $z \approx 8$ galaxies with $M_{s} \approx 10^{9} M_{\odot}$, in Labbé et al. (2013), appearing as an excess in the IRAC [4.5] band. The implied equivalent width for their sample is $EW_{\nu}(\text{[O III]}) + H\beta = 670 \AA$. Thus, we conclude that although very strong [O III]-emitting galaxies are rare in the local universe, they become increasingly common from redshifts $1 < z < 2$, to $2 < z < 3$. At higher redshifts, very strong [O III] emitters may even become the norm.

Aside from the $K$-band excess, we observe two more subtle features in the faint average LBG SEDs in Figure 8 that are not explained by the best-fit stellar models. First, there is an excess in the $J$-band flux over the stellar continuum. An analogous feature has been found in stacked SEDs of $z \approx 4$ galaxies in González et al. (2012), in the form an $H$-band excess. These authors attribute the excess to a bias due to the Balmer break falling into the $H$-band for the low-redshift tail of their sample, such that the stacked $H$-band flux is increased by flux redward of the break for the lower-redshift tail of their sample. However, our LBG selection is not sensitive to the low redshifts required for this bias to explain the observed stacked $J$-band excess. An alternate contribution to the observed $J$-band excess in our faint LBG SEDs might come from bound-free and free-free nebular continuum emission at rest-frame $\sim 3100 \AA$. We predict the possible contribution from nebular continuum emission at these wavelengths by assuming a typical [O III]/$H\beta = 3$ to estimate the $H\beta$ flux from the [O III] equivalent widths. Using the tabulated $H\beta$ and continuum emission coefficients at an electron temperature of $T_{e} = 10,000$ K from Osterbrock (1989), we determine that the nebular continuum can contribute $\sim 10\%$ to the observed $J$-band flux. This would still leave about $20\%$ of the observed flux in the faintest bin unaccounted for. We thus conclude that the $J$-band excess is largely due to uncertainty in forming the stacked images, such as an over-correction for the faint-stack defect described in Section 5.1.1. Another uncertainty comes from our assumption of a simple stellar population to describe the starlight.

There is also weak evidence of Ly$\alpha$ line emission increasing $V$-band flux in the faintest LBGs ($(\langle \alpha \rangle = 27$). Comparing the observed $V$ flux to the flux predicted by convolving the stellar continuum model with the $V$ filter transmission profile yields an excess of $\approx 2\sigma$ significance, and implies a Ly$\alpha$ equivalent width of $EW_{\nu}(\text{Ly}\alpha) \approx 30 \AA$. If correct, this would mean that most of the LBGs in the faintest stack are Ly$\alpha$ emitters (LAEs). This would be consistent with the increasing LAE fraction found in the faintest LBGs at $3 < z < 7$ (Stark et al. 2010, 2011; Pentericci et al. 2011; Ono et al. 2012; Schenker et al. 2012; Treu et al. 2012). However, those studies generally do not include galaxies fainter than $M_{V} = -18.75$, while the LBGs in our sample extend to lower luminosity. Nonetheless, if we extrapolate the result from Stark et al. (2010) down to absolute magnitude $M_{V} \approx -18$, this would predict that $\sim 70\%$ of LBGs at $3 < z < 6.3$ should be LAEs with $EW_{\nu}(\text{Ly}\alpha) > 50 \AA$. Our observed average $30 \AA$ equivalent width could be explained if about half of the faintest LBGs are strong LAEs with $EW_{\nu}(\text{Ly}\alpha) > 50 \AA$. Alternatively, a few bright sources in the faint bin might have extremely strong Ly$\alpha$ emission, with the rest having weak or no emission (or perhaps even absorption). This would be consistent with what is observed for bright LBGs (Shapley et al. 2003, for example); however, we are in the regime of faint dwarf galaxies with little extinction from dust.

5.3.2. [O III] Line Ratios and ISM Conditions

The physical conditions of star-forming regions at high redshift differ significantly from local systems. An observable consequence of these differences is higher [O III]/$H\beta$ and [O III]/$H\alpha$ ratios measured in distant versus local galaxies (e.g., Teplitz et al. 2004; Shapley et al. 2005; Erb et al. 2006; Ly et al. 2007a; Brinchmann et al. 2008; Liu et al. 2008; Schenker et al. 2013; Steidel et al. 2014; Sanders et al. 2015; Holdén et al. 2016). To place the LBGs studied here in this context, we estimate [O III]/$H\alpha$ ratio using the implied EW([O III]) and best-fit SFRs of the stacked LBGs. The [O III] luminosity is calculated from

$$ L_{\text{[O III]}} = 4\pi D_{L}^{2} f_{\text{[O III],cont}} \times EW([\text{O III}]), \quad (11) $$

where $D_{L}(z = 3.1) = 26$ Gpc is the luminosity distance at $z = 3.1$, $f_{\text{[O III],cont}}$ is the continuum flux density at $2.2 \, \mu m$ in ergs $s^{-1} \, cm^{-2} \, \AA^{-1}$ (measured from the best-fit stellar continuum model as described above), and the equivalent widths are in the observed frame.

We estimate the $L_{H\alpha}$ of the LBGs from their model SEDs with the same approach used in Ly et al. (2012). We use the Kennicutt (1998) relation to calculate intrinsic $H\alpha$ luminosity from the best-fit SFRs: $L_{H\alpha,int} = 1.26 \times 10^{41}$ SFR $[M_{\odot} \, yr^{-1}]$. Then, in order to compare our LBGs with other galaxy samples, we predict their reddened $H\alpha$ luminosities by estimating the extinction for the $H\alpha$ line, $A(H\alpha)$, from their best-fit visual extinction $A_V$. The $H\alpha$ extinction can be written in terms of an extinction curve evaluated at $\lambda = 6563 \, \AA$, $k(6563 \, \AA)$, and the color excess for the gas $E(B - V)_{\text{gas}}$:

$$ A(H\alpha) = k(6563 \, \AA) \times E(B - V)_{\text{gas}}. \quad (12) $$

For simplicity, we adopt $k(6563 \, \AA) = 2.00$ from the SMC extinction curve (Gordon et al. 2003). We relate the color excess for the gas to that for the stellar continuum by assuming the Calzetti et al. (2000) relation: $E(B - V)_{\text{gas}} = 2.27 E(B - V)_{\text{stars}}$. We note that previous studies generally support the assumption that the extinction for the gas is roughly twice that of the stars (e.g., Ly et al. 2012; Reddy et al. 2015). Thus:

$$ A(H\alpha) = k(6563 \, \AA) \times 2.27 \times E(B - V)_{\text{stars}}, \quad \text{A(H}\alpha) = 4.54 \times E(B - V)_{\text{stars}}. \quad (13) $$

The color excess for the stars is calculated assuming the Calzetti attenuation law: $E(B - V)_{\text{stars}} = A_V / 4.05$. We note that regardless of our assumptions for the reddening of $H\alpha$, the results discussed below are not significantly impacted ($\lesssim 0.1$ dex difference).

We plot estimated $L_{H\alpha}$ versus $L_{\text{[O III]}}$ for the average LBG SEDs in Figure 11. The black dashed-dotted line indicates a slope of unity ($[\text{O III]}/H\alpha = 1$). The average $\langle \alpha \rangle = 25, 26,$ and 27 stacked LBGs have $[\text{O III]}/H\alpha \approx 1.6, \ 3.1, \text{ and } 4.1$, respectively. The solid black line and gray band represent the
mean relation and scatter for WISP galaxies in the redshift range $z = 0.8$–1.2 reported in Mehta et al. (2015). Our two faintest stacked SEDs lie toward the bottom edge of the scatter, comparable to the more extreme WISP galaxies observed. Likewise, $[\text{O III}]/\text{H}$ in the faint LBGs is consistent with the ratios observed for a subset of WISP galaxies with Magellan/FIRE spectra in Masters et al. (2014), which reach $[\text{O III}]/\text{H} \propto 3$ (shown on the plot as yellow triangles). Domínguez et al. (2013) reports line ratios for stacked WISP spectra reaching an average $[\text{O III}]/\text{H} \approx 2$ for their faintest bin of $L_{\text{H}}$. At $z \approx 2.3$, galaxies from the MOSDEF survey have stacked spectra (binned by mass) indicating a maximum average $[\text{O III}]/\text{H} \approx 1.8$ (Sanders et al. 2015). However, these stacks (shown as orange triangles in the plot) were normalized by $L_{\text{H}}$, which prevents low-metallicity objects with high $[\text{O III}]/\text{H} \beta$ from dominating the stacked line ratios. The most extreme galaxies at $z \approx 1.95$–2.65 in the KBSS survey (Steidel et al. 2014) have individual spectra that reach up to $[\text{O III}]/\text{H} \approx 4$. The $z \lesssim 1$ ELGs from Ly et al. (2015) and Ly et al. (2016), also included in Figure 11, form a locus with a shallower slope than the faint stacked LBGs. Perhaps most comparable to our sample is a subset of six “extreme” green peas (Jaskot & Oey 2013) that have $[\text{O III}]/\text{H} \approx 3.0$ on average (shown as the green circles in the plot).

The average faint galaxy in our sample is clearly efficient at converting ionizing photons from starlight into $[\text{O III}]$ emission. By integrating the stellar continuum models fit to the faint average LBGs, we estimate the ratio of flux in $[\text{O III}]$ to observed (reddened) stellar luminosity. The ratio is $1\%$ for $i' = 26$ and $\approx 3\%$ for $i' = 27$ stacked LBGs. Spectroscopic surveys of high-redshift galaxies such as those described above support this trend of high-level $[\text{O III}]$ emission in the distant universe. Theoretical explanations include the possibility that the interstellar medium (ISM) has a larger ionization parameter (ionizing photon density to gas density), higher electron density, harder ionizing radiation spectrum, and/or very low metallicity (e.g., Kewley et al. 2013a, 2013b; Steidel et al. 2014; Nakajima & Ouchi 2014; Sanders et al. 2016). The very strong $[\text{O III}]$ emission implied for the average faint LBG in this study suggests that extreme ionization conditions (relative to those found in most local galaxies) are ubiquitous in low-mass galaxies at $z \approx 3$. Recent studies have shown that green peas (local strong $[\text{O III}]$-emitters), which have ISM properties similar to LBGs, are good candidates for leaking a significant amount of ionizing radiation (e.g., Nakajima & Ouchi 2014; Izotov et al. 2016a, 2016b). Thus, galaxies at $z > 6$ that are directly analogous to the faint LBGs in this study might have been responsible for the bulk of the cosmic reionization of the intergalactic medium. Confirmation will require deep spectroscopy at wavelengths of 3.5 μm or longer. This will be possible with the James Webb Space Telescope in targeted surveys, or serendipitously with slitless spectroscopy.

6. LBG Clustering in the SDF

Clustering analysis requires highly uniform sensitivity over a large contiguous area, because fluctuations of sensitivity can produce spurious clustering signals and bias the measurements of clustering strength. We examined the sensitivity variation over the images by dividing them into small grids and estimating the sky noise in each of the meshes. Based on these sky-noise maps, we carefully defined a high-quality region in which the sensitivity is good and uniform, trimming the edges of the images where sky noise was systematically larger due to dithering. The effective area with complete coverage in all of the six optical bands and the $K$-band amounts to 876 arcmin$^2$, after low-quality regions are discarded, including the edges. Figure 12 shows the sky distribution of the LBG sample. Larger red circles denote objects that have brighter $R_c$-band magnitudes.

Figure 11. Reddened $L_{\text{H}}$ from the LBG SFRs vs. $L_{\text{[O III]}}/\lambda 4959,5007$, derived from their implied equivalent widths, compared to other samples of emission-line galaxies (see Section 5.3.2 for description of samples).

Figure 12. Sky distribution of the LBGs in our sample. The red circles ordered from largest to smallest represent LBGs with $23.0 < R_c < 24.5$, $24.5 < R_c < 25.5$, $25.5 < R_c < 26.5$, and $26.5 < R_c < 27.5$, respectively. The projected comoving scale of 10 Mpc at $z = 3.3$ is shown in the bottom center. North is up and east is to the left in this image.
Figure 13. Observed ACFs for the total (black) and bright (red) U-dropout galaxies. The solid lines represent the best-fit ACFs calculated by the HOD model.

6.1. Angular Correlation Function

We measure the clustering of both our LBG sample as a whole (all 5161 objects), and the brightest half of the sample (split by $R$-magnitude), in order to investigate mass-dependent clustering. We largely follow the methodology of Yoshida et al. (2008) to calculate the angular correlation function (ACF), $\omega(\theta)$, using the Landy & Szalay (1993) estimator:

$$\omega(\theta) = \frac{dd(\theta) - 2dr(\theta) + rr(\theta)}{rr(\theta)},$$  

where $dd(\theta)$, $dr(\theta)$, and $rr(\theta)$ are the numbers of galaxy–galaxy, galaxy–random, and random–random pairs, respectively, with angular separations $\theta$. In creating the random catalog, we avoided regions where galaxies are not detected (for example, near bright stars). We generated a factor of 100 more random coordinates than the number of galaxies in the sample, and normalized $dd$, $dr$, and $rr$ to the total number of pairs. Because the random pairs are subject to the same limitations as the real data, the deficiency of faint galaxies we found within several arcseconds of other galaxies due to confusion should not impact our estimated clustering.

We evaluate errors and covariance matrices of both the full sample and bright-half sample by the delete-one jackknife resampling method. The entire survey field is divided into 36 subfields and ACFs are calculated by omitting one subfield, repeating this procedure 36 times. The covariance matrix, $C_{ij}$, is derived as

$$C_{ij} = \frac{N}{N-1} \sum_{k=1}^{N} (\omega_k(\theta_i) - \bar{\omega}(\theta_i)) \times (\omega_k(\theta_j) - \bar{\omega}(\theta_j)),$$  

where $\bar{\omega}(\theta)$ is the averaged ACF of the $i$th angular bin.

The observed ACFs and associated error bars for the bright and full samples of LBGs are shown in Figure 13.

6.2. Halo Occupation Distribution

At separations smaller than $\approx 10''$, corresponding to about 80 kpc at $z = 3$, the observed ACFs in Figure 13 show a significant steepening. Such a steepening has also been found in previous LBG clustering studies, and is attributed to the additional clustering of $>1$ galaxies residing in a single dark matter halo (Hildebrandt et al. 2007; Yoshida et al. 2008; Bielby et al. 2013; Bian et al. 2013). Thus, rather than fit a single power-law to the ACF, as is commonly done, we carried out a halo occupation distribution (HOD; e.g., Berlind & Weinberg 2002; Zheng et al. 2005; van den Bosch et al. 2007) analysis to interpret the relationship between the $U$-dropout galaxies and their host dark halos. We employ the standard halo occupation model proposed by Zheng et al. (2005). The occupation of central galaxies, $N_c(M_h)$, is formulated as

$$N_c(M_h) = \frac{1}{2} \left[ 1 + \text{erf} \left( \frac{\log(M_h) - \log(M_{\text{min}})}{\sigma_{\log M}} \right) \right],$$

whereas the occupation of satellite galaxies, $N_s(M_h)$, can be described by:

$$N_s(M_h) = \left( \frac{M_h - M_{\text{crit}}}{M_1} \right)^\alpha.$$

The number of total galaxies within dark halos with mass $M_h$ is:

$$N(M_h) = N_c(M_h)[1 + N_s(M_h)].$$

We vary all of the HOD free parameters, $M_{\text{min}}$, $M_1$, $M_{\text{crit}}$, $\sigma_{\log M}$, and $\alpha$, and find the best-fit parameters to the observed ACFs.

The HOD analysis requires assuming some analytical models to characterize dark halos. We use the halo mass function of Sheth & Tormen (1999), the radial density profile of Navarro et al. (1997), the halo bias model of Tinker et al. (2010), and the halo mass-concentration parameter relation of Takada & Jain (2003). The redshift completeness functions $p(m, z)$ (Section 3.3) are employed as the redshift distributions of each subsample.

The HOD parameters are constrained through minimizing the $\chi^2$ as follows:

$$\chi^2 = \sum_{i,j} (\omega_{\text{obs}}(\theta_i) - \omega_{\text{HOD}}(\theta_i))(C^{-1})_{ij}(\omega_{\text{obs}}(\theta_j) - \omega_{\text{HOD}}(\theta_j)) + \frac{(n_{\text{obs}} - n_{\text{HOD}})^2}{\sigma_n^2},$$

where $C^{-1}$ is the inverse covariance matrix (Equation (15)), $n_{\text{obs}}$ and $n_{\text{HOD}}$ are the galaxy number densities from observation and the HOD model, and $\sigma_n$ is the statistical 1$\sigma$ error of $n_{\text{obs}}$, respectively. The best-fit parameter sets and those 1$\sigma$ confidence intervals are estimated by Markov Chain Monte Carlo simulation. We note that effects of contaminations on observed ACFs are corrected by multiplying the factor of $1/(1 - f_c)^2$, where $f_c$ represents the fraction of contamination.

The best-fit ACFs for the full and bright LBG samples, computed by the HOD modeling, are shown with the observed ACFs in Figure 13. The best-fit HOD parameters and deduced parameters, i.e., mean halo masses and satellite fractions, are listed in Table 5. Mean halo masses, $\langle M_h \rangle$, and satellite fractions, $f_{\text{sat}}$, are defined as

$$\langle M_h \rangle = \frac{\int dm_h m_h n(M_h)N(M_h)}{\int dm_h n(M_h)N(M_h)},$$

where $m_h$ is the halo mass for a given redshift and $n(M_h)$ is the halo mass function.
and
\[ f_{\text{sat}} = 1 - \frac{\int dM_h n(M_h) N_0(M_h)}{\int dM_h n(M_h) N_0(M_h)}, \]

where \( n(M_h) \) is the halo mass function.

The mean halo masses implied for the total LBG sample and bright-half subsample are \( \langle M_h \rangle = (1.9^{+0.6}_{-0.5}) \times 10^{11} h^{-1} M_\odot \), and \( \langle M_h \rangle = (3.1^{+0.8}_{-0.6}) \times 10^{11} h^{-1} M_\odot \), respectively. Bian et al. (2013) have also carried out HOD analysis for their \( z \sim 3 \) LBG sample in two magnitude bins and found \( \langle M_h \rangle = (2.5 \pm 0.3) \times 10^{12} h^{-1} M_\odot \) for LBGs with \( 24.0 < R < 24.5 \), and \( \langle M_h \rangle = (3.3^{+0.6}_{-0.4}) \times 10^{12} h^{-1} M_\odot \) for \( 23.5 < R < 24.0 \). The mean halo masses derived for our sample of LBGs are significantly smaller, consistent with the fact that we include much fainter galaxies in the sample (down to \( R \approx 28 \) for the full sample).

Overall, the HOD analysis of our LBG sample and comparison to that of brighter samples support the notion that more massive dark matter halos host more luminous LBGs.

7. Summary

Using deep multi-waveband imaging data from optical to infrared wavelengths in the Subaru Deep Field, we investigate the LF, physical properties, and clustering of a large sample of Lyman-break galaxies (LBGs) at \( z \sim 3 \). The LBGs are selected by \( U - V \) and \( V - R_c \) colors in one contiguous area of 876 arcmin\(^2\) down to \( R_c = 27.8 \), yielding a sample of 5161 LBGs in total. A subset of 140 of these LBGs are detected in near-infrared wavelengths (in both \( H \) and \( K \) band). We use Monte Carlo simulations to estimate the redshift distribution function and fraction of contamination by interlopers of the LBG samples. As expected, our LBG search is fairly uniformly sensitive to redshifts between \( z = 2.9 \) and 3.5, with a declining tail to higher redshifts.

Using our completeness simulations, we calculate the LBG LF and find that our results are broadly consistent with previous LF determinations at \( z \sim 3 \). We fit our LBG LF with a standard Schechter function, deriving a steep faint end slope of \( \alpha = -1.78 \pm 0.05 \) and characteristic magnitude of \( M_V^{0.05} = -20.86 \pm 0.11 \). We also measure clustering for the LBG sample and model the angular correlation function using the halo occupation distribution framework. We find that, on average, the bright half of the LBG sample resides in more massive dark matter halos than the sample as a whole. This suggests that more-luminous LBGs (which host a larger star formation rate) reside in more massive dark matter halos.

To infer physical properties of the LBGs, we construct their average rest-frame UV-to-NIR (observed optical to mid-IR) SEDs. The SEDs are generated by binning our sample according to \( i' \)-magnitude and obtaining stacked LBG detections in the infrared by median-averaging at the optical positions of the LBGs. Stacking is performed in WFCAM \( J \), \( H \), and \( K \) bands through IRAC [3.6], [4.5], [5.8], and [8.0] \( \mu \)m filters. In the stacks of faint LBGs, we find a background depression in the immediate vicinity of the stacked object. We confirm that this background deficit is due to the source detection algorithm, SExtractor, preferentially selecting only faint galaxies that happen to fall in regions of low background counts (they are relatively isolated in the nearly confusion-limited data). We suggest that most (if not all) catalogs generated from similar detection routines suffer from this bias. Thus, stacks of objects in such catalogs should be appropriately corrected for the locally faint background.

We applied these corrections to all faint stacked images prior to measuring fluxes. The average LBG SEDs are then formed by combining the median \( UBVRi'cz' \) photometry with photometry from the corrected stacked images. We fit the average SEDs with stellar population synthesis templates and infer stellar mass and SFRs, among other properties. The average LBGs range in stellar mass from \( \zeta 10^{10} M_\odot \) down to \( \zeta 10^{8} M_\odot \), and are forming stars at rates of \( 50 M_\odot \) yr\(^{-1} \) to \( 3 M_\odot \) yr\(^{-1} \), from bins of \( i' = 24 \) to \( i' = 27 \), respectively. The properties are generally consistent with other samples of LBGs at this redshift and lie close to the “star-forming main sequence” at \( z \sim 3 \).

The average SEDs for the faint, low-mass bins have additional features that are indicative of strong nebular emission. There is a large excess in the \( K \)-band flux that we attribute to the contribution of \( [O \text{ III}] \lambda \lambda 4959,5007 + H\beta \) emission. From the excess, we estimate rest-frame equivalent widths reaching \( EW_{\text{obs}}([O \text{ III}]) \sim 1000 \) \( \AA \) for the faintest magnitude bin \( (i') = 27 \). This result suggests that the average low-mass galaxy that is forming stars at \( z \sim 3 \) radiates a large fraction of its power, \( \sim 1\% \) or more of the total stellar luminosity, in this \( [O \text{ III}] \) doublet. Furthermore, this efficiency in \( [O \text{ III}] \) emission increases as galaxy stellar mass decreases and sSFR increases. Strongly star-forming dwarf galaxies can thus be detected by the excess brightness produced by \( [O \text{ III}] \lambda \lambda 4959,5007 \) in their broad-band SEDs, even if they are too faint for spectroscopy.

The faint average LBGs are comparable to the most extreme emission-line galaxies at lower redshift. The result appears plausible in the context of emerging evidence for ubiquitous strong \( [O \text{ III}] \) emission in the high-\( z \) universe. Recently, there have been discoveries of significant leakage of ionizing radiation from green pea galaxies, which are local analogs of \( [O \text{ III}] \)-emitting LBGs. We suggest that low-mass systems with strong \( [O \text{ III}] \) emission, which are seemingly pervasive in the high-redshift universe, are strong candidates to produce the bulk of cosmic reionization at \( z > 6 \).

This study of 5161 \( U - V \) dropouts LBGs yields some results consistent with other studies of star-forming galaxies at \( z \sim 3 \). However, we were surprised to find such strong and widespread \( [O \text{ III}] \) emission in the average (faint, i.e., typical) LBGs. Telescopes like the Wide-Field Infrared Survey Telescope and the James Webb Space Telescope, will undoubtedly utilize strong \( [O \text{ III}] \) emission lines to characterize the typical galaxies at \( z > 3 \) (Colbert et al. 2013). This doublet could prove at least as important as Ly\( \alpha \), or even more so, in studying those galaxies that likely re-ionized the universe. One positive conclusion is that, as the infrared spectroscopic searches push deeper, they will benefit more and more from
the relative ease of detecting [O III] lines in the fainter galaxies. One
concern is that surveys of large-scale structure based on [O III] line emission will be strongly biased toward the least
massive galaxies, which may have relatively weaker clustering.

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