Uplink interference protection and scheduling for energy efficient OFDMA networks

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Abstract
One of the key challenges for future orthogonal frequency division multiple access-based networks is inter-cell interference coordination. With full frequency reuse and small inter-site distances, coping with co-channel interference (CCI) in such networks has become increasingly important. In this article, an uplink interference protection (ULIP) technique to combat CCI is introduced and investigated. The level of uplink interference originating from neighbouring cells (affecting co-channel mobile stations (MSs) in the cell of interest) can be effectively controlled by reducing the transmit power of the interfering MSs. This is done based on the target signal-to-noise-plus-interference ratio (SINR) and tolerable interference of the vulnerable link. Bands are prioritised in order to differentiate those (vulnerable/victim) MSs that are to be protected from interference and those (aggressor/interfering MSs) that are required to sacrifice transmission power to facilitate the protection. Furthermore, MSs are scheduled such that those users with poorer transmission conditions receive the highest interference protection, thus balancing the areal SINR distribution and creating a fairer allocation of the available resources. In addition to interference protection, the individual power reductions also serve to decrease the total system uplink power, resulting in a greener system. It is shown through analytic derivation that the introduction of ULIP guarantees an increase in energy efficiency for all MSs, with the added benefit that gains in overall system throughput are also achievable. Extensive system level simulations validate these findings.

Keywords: inter-cell interference coordination, uplink interference protection, OFDMA networks, fair scheduling

1. Introduction
In wireless networks, there is an increasing demand for higher user and system throughput, along with growing expectation for all mobile stations (MSs) in a cell to be capable of supporting data-heavy multimedia and Internet services. This is especially difficult to maintain at the cell-edge, where received signal and service clearly deteriorate. Furthermore, the necessity for more energy efficient, or “green,” technologies is growing. With base stations (BSs) requiring up to 1.5 kW, a typical wide area network can consume tens of MW per annum [1]. In the uplink, while MSs do not consume nearly as much power, there are orders of magnitude more MSs than BSs in the network [2]. In addition with traffic loads increasing approximately ten times every 5 years, a doubling of the energy consumption results over the same period time. Clearly, such an increase raises serious environmental concerns. Consequently, smaller cell sizes, femto-cell deployment, relays [3,4] and especially inter-cell interference coordination (ICIC) techniques are envisioned for future wireless networks to improve user throughputs and network energy efficiency, while sacrificing minimal system capacity.

For future wireless networks, such a reduction in cell size is undertaken due to transmit power limitations and constraints on the link budget [5]. The demand for higher data rates coupled with full frequency reuse results in an interference-limited system, which cannot achieve full capacity without the implementation of one or more viable interference mitigation/cancellation/coordination techniques [5]. Furthermore, through the implementation of orthogonal frequency division multiple access (OFDMA) in the downlink and single carrier frequency division multiple access (SC-FDMA) in the uplink as multiple access schemes, future systems will provide orthogonality between resource blocks (RBs) in both directions, and hence also between all users within...
a cell [2]. Thus, system performance is mainly limited by interference originating from users in neighbouring cells, which can be detrimental to the signal-to-noise-plus-interference ratio (SINR) and throughput performance of MSs using the same RBs [6]. A typical solution is to force interferers to leave those RBs idle. However, this severely harms the trunking efficiency of the network [7]. Hence, suppressing transmission is clearly suboptimal, and thus interference coordination techniques are necessary to achieve desired sum and individual throughputs.

For OFDMA systems, some traditional ICIC techniques, such as power control, interference cancellation, fractional frequency reuse, multiple-input multiple-output transmission and space division multiple access [2], have been proposed. Some of these strategies, however, require knowledge about the position of a MS relative to its own and neighbouring BSs [2], which clearly increases the signalling burden in the network. In [8], other specific ICIC techniques are suggested, such as slow power control, frequency division multiplexing resource allocation, and coordination by MS alignment, though management of interference from other cells is not considered. Further research in [9] presents a distributed uplink power allocation technique based on a maximum sum rate optimisation, yielding superior results in terms of average system throughput, however ignoring the tradeoff between cell-edge performance and overall spectral efficiency. In [10], a softer frequency reuse scheme is introduced, where cell-edge power masks are used to mitigate inter-cell interference. These fixed masks cannot, however, adapt to the service-dependent requirements of the neighbouring cells, potentially wasting bandwidth. In [11], the downlink scheduling is formulated as an optimisation problem, and a decomposition of the problem is performed. Here, however, co-channel interference (CCI) (in future systems from neighbouring cells) is not taken into account, and hence the scheduling becomes suboptimal for multiple access channels and large networks.

In [12], a dynamic channel acquisition algorithm based on convex optimisation for the wireless downlink is considered, which provides optimal power and throughput performance for i.i.d. channels. This optimality suffers however for general ergodic channels, and hence is not suitable for mobile environments. In [13], the authors propose a low-complexity algorithm with fairness consideration to optimise the sum rate under individual rate and power constraints. Here though, because the water-filling solution is used for rate-optimal power allocation, a fair power distribution is neglected. In [14], an optimisation-based heuristic inter-cell coordination scheme is proposed to regulate the uplink transmission in neighbouring cells such that inter-cell interference is mitigated. As the scheme operates iteratively on a two-cell basis, however, it is clearly unsuitable for multi-cellular resource allocation. Finally, in [15], an energy-aware cross-layer radio management framework is proposed, that partitions the global optimisation problem into subproblems, which can be solved locally. While achieving substantial gains, the focus of the work is on multimode communication (i.e., cellular, WLANs, WMANs, etc.), and so an optimisation for pure cellular communication is not offered. In general, it is evident that the challenge of resource and power allocation has been thoroughly investigated as an optimisation problem, however in most cases these problems are non-convex, very hard to solve, and hence suboptimal heuristics are developed. In this work, a resource and power allocation technique based on local interference requirements will be developed to manage this challenge.

Much of the previous work on energy efficient systems concentrates on network optimisation and scheduling policies. Macro-cell size reduction for better energy efficiency is investigated in [16], with positive results. Of course, reducing the cell-sizes means increasing the number of BSs in an area, which is generally rejected due to the enhanced infrastructure expenses. In [17], game-theoretic approaches are utilised to, minimise the cost per reliable bit sent in energy constrained networks. However, it is seen that there is a clear tradeoff between energy and spectral efficiency, and hence the energy-efficient resource allocations tend to be spectrally inefficient. This is further highlighted in [18], where an analytical model determines the optimal energy-spectral efficiency tradeoff for the downlink in OFDMA networks. In this article, however, we present an ICIC technique which utilises interfering link gains to not only provide interference mitigation and spectral efficiency gains in the uplink, but also generate large energy savings.

An energy efficient interference protection technique for the uplink of OFDMA-based systems is introduced. By reducing the power on the interfering link, the SINRs of individual RBs can be enhanced. This power reduction also results in a more energy efficient system. By segregating the spectrum into priority bands, MSs allocated lower priority RBs provide interference protection for higher priority RBs in neighbouring cells by decreasing their transmit power. The priority bands (i.e., low to high) are allocated such that the same RBs in any neighbouring cells do not share the same priority class, and hence a priority reuse scheme [19] is established. Furthermore, the proposed power reduction is based on target SINRs, providing real-time service-dependent interference coordination and energy efficiency in the uplink.

The rest of the article is structured as follows: Section 2 describes the system and channel environment, Section 3 explains the uplink interference protection (ULIP) protocol and its performance in wireless networks is analysed.
in Section 4. In Sections 5 and 6 the resource scheduler and simulation are described, respectively. Finally, Section 7 portrays and discusses the simulation results, and some concluding remarks are offered in Section 8.

2. System and channel model B/M

The reverse link of an OFDMA system is considered, where the system bandwidth \( B \) is divided into \( M \) RBs. A RB defines one basic time-frequency unit of bandwidth \( B_{\text{RB}} = \eta B \). All MSs can transmit up to a maximum power \( P_{\text{max}} \) and hence up to \( P_{\text{max}}M \) on each RB. Perfect time and frequency synchronisation is assumed.

Universal frequency reuse is considered, so that each macro-cell utilises the entire system bandwidth. The set of RBs \( M \), where \( |M| = M \), is distributed by each BS to its associated MSs. Throughout this article, \( u \) is used to define any MS, and \( v_u \) the BS with which this MS is associated. The received signal observed by BS\( v_u \) from MS\( u \) on RB\( m \) is given by

\[
Y_u^m = \frac{P_u^m C_{u,v_u}^m}{\eta} + I_u^m + \eta,
\]

(1)

where \( C_{u,v_u}^m \) denotes the channel gain between the MS\( u \) and its serving BS\( v_u \), observed on RB\( m \). Furthermore, \( I_u^m \) denotes the transmit power of MS\( u \) on RB\( m \), \( S_u^m \) the desired received signal, \( \eta \) the thermal noise, and \( I_u^m \) the CCI received on RB\( m \) from MSs in neighbouring cells. The interference \( I_u^m \) is defined by

\[
I_u^m = \sum_{k \in \mathcal{I}_u} P_{k,v_u}^m C_{u,k}^m,
\]

(2)

where \( \mathcal{I}_m \) represents the set of interferers (i.e., the set of MSs in neighbouring cells that are also assigned RB\( m \)). Hence, the SINR observed at the BS\( v_u \) on RB\( m \) is calculated by

\[
\gamma_u^m = \frac{S_u^m}{I_u^m + \eta} = \frac{P_u^m C_{u,v_u}^m}{\sum_{k \in \mathcal{I}_u} P_{k,v_u}^m C_{u,k}^m + \eta}.
\]

The achievable throughput on the link between MS\( u \) and BS\( v_u \) on RB\( m \) using adaptive modulation and coding (AMC) is given by

\[
C_u^m(\gamma_u^m) = k_{sc} Q_s \varepsilon_s(\gamma_u^m) \left[ \frac{\text{bits/s}}{\text{RB}} \right],
\]

(4)

where \( k_{sc} \) is the number of subcarriers per RB, \( Q_s \) the symbol rate per subcarrier, and \( \varepsilon_s(\gamma_u^m) \) the symbol efficiency given in Table 1.a

Further, \( C_u \) denotes the achievable throughput of MS\( u \), and is calculated by the aggregate throughput achieved on the RBs assigned to MS\( u \)

\[
C_u = \sum_{m \in \mathcal{M}_u} C_u^m = \sum_{m \in \mathcal{M}_u} k_{sc} Q_s \varepsilon_s(\gamma_u^m) \left[ \frac{\text{bits}}{s} \right],
\]

(5)

where \( \mathcal{M}_u \) describes the set of RBs assigned to MS\( u \) in the current transmission, and \( \varepsilon_s^m = \varepsilon_s(\gamma_u^m) \). Finally, the system capacity is calculated as the sum of achievable throughput of all MSs

\[
C_{\text{sys}} = \sum_u C_u.
\]

(6)

The energy efficiency \( \beta_u \) measures the data sent per unit of energy (or, alternatively, data rate per unit of transmit power) of MS\( u \). This is defined as follows:

\[
\beta_u = \frac{C_u}{P_u} = \frac{\sum_{m \in \mathcal{M}_u} k_{sc} Q_s \varepsilon_s(\gamma_u^m)}{\sum_{m \in \mathcal{M}_u} P_{m,u}^m} \left[ \frac{\text{bits/s}}{\text{W}} \right] = \left[ \frac{\text{bits}}{\text{J}} \right],
\]

(7)

where \( P_u \) is the total transmit power of MS\( u \), and \( C_u \) the throughput from (5).

Lastly, Jain’s fairness index [20] is used to calculate the throughput fairness of the system in each time slot (i.e., Long-Term Evolution (LTE) subframe)

\[
\Gamma(k) = \frac{\sum_u C_u(k)}{N_{\text{sys}} \sum_u C_u(k)},
\]

(8)

where \( k \) indicates the time slot, \( N_{\text{sys}} \) the number of MS in the system, and \( C_u(k) \) the achieved throughput of MS\( u \) over all time slots 1: \( k \).
2.1. Channel model
In general, the channel gain, $G_{kl}^m$, between a transmitter $k$ and receiver $l$, observed on RB$_m$ and separated by $d$ m is determined by the path loss, log-normal shadowing, and channel variations caused by frequency-selective fading:

$$G_{kl}^m = |H_{kl}^m|^2 10^{-\frac{L(d)}{10} X_v},$$  \hspace{1cm} (9)

where $H_{kl}^m$ describes the channel transfer function between transmitter $k$ and receiver $l$ on RB$_m$. $L(d)$ is the distance-dependent path loss (in dB) and $X_v$ is the log-normal shadowing value (in dB) with standard deviation $\sigma$, as described in [21]. The channel generally exhibits time and frequency dispersions, however channel fluctuations within a RB are not considered as the RB dimensions are significantly smaller than the coherence time and frequency of the channel [22]. Furthermore, the large-scale path loss $L(d)$ is identical on all RBs assigned to a MS. Finally, the delay profiles used to generate the frequency-selective fading channel transfer factor $H_{kl}^m$ are taken from applicable propagation scenarios in [21,23].

The path loss model used to calculate $L(d)$ is for a purely outdoor link [24], i.e., the link (desired or interfering) between a BS and an outdoor MS, and calculates the path loss as

$$L(d) = 15.3 + 37.6 \log_{10}(d) \hspace{1cm} [\text{dB}],$$  \hspace{1cm} (10)

where $d$ is the distance between transmitter and receiver.

Log-normal shadowing is added to all links through the use of correlated shadowing maps. These are generated such that the correlation between two points is distance-dependent.

3. Uplink interference protection (ULIP)
Traditional uplink power control methods use the estimated path gain on the intended link to perform MS transmit power adaptation [25,26]. A better option is to utilise the interfering link, i.e., to a neighbouring BS, to reduce the transmit power on the affected RBs, such that interference caused to neighbouring BSs is lessened. This way, vulnerable MSs in the cell of interest have a chance of maintaining sufficient SINR, while the offending links remain active.

3.1. Uplink interference scenario
Figure 1 portrays the interference scenario of two MSs in the uplink.

Here, the vulnerable MS, served by BS$_v$, and the interfering MS, served by BS$_i$, are transmitting on the same RB. Due to the uplink interference at BS$_i$, caused by MS$_i$, the SINR of MS$_v$ may fall below the SINR target, $\gamma_v^\text{tar}$. To prevent such a situation, an interference protection technique is devised that reduces the transmit power $P_i$ such that MS$_v$ achieves a satisfactory SINR, $\gamma_v \geq \gamma_v^\text{tar}$.

3.2. Interference aware power reduction
The goal is to find an effective method to scale the transmit power on the interfering RBs. Here, the downlink reference signal of the neighbouring cells aid the MS in estimating the interference it causes to the neighbouring cells, assuming channel reciprocity. The channel can be considered reciprocal in terms of path loss and shadowing, however fast fading reciprocity is not assumed as this is not always the case, especially in frequency division duplex (FDD) systems. For LTE, the reference signal received power (RSRP) in particular is used. The RSRP provides a cell-specific signal strength metric. It is used mainly to rank different cells according to signal strength and to perform handover and cell reselection decisions [27]. The reference signals facilitate the adaptation of the interfering RB transmit power, which is performed as follows:

1. Assume MS$_v$ has been allocated the vulnerable RB$_m$. Let $\gamma_v^\text{tar}$ be the known, service-dependent target SINR of MS$_v$, calculated as

$$\gamma_v^\text{tar} = \frac{P_m v G_{vv}^m}{P_m v I_{v,tot}^m + N},$$  \hspace{1cm} (11)

where $P_m v$ is the transmit power on RB$_m$, $G_{vv}^m$ is the path gain between MS$_v$ and its BS$_{vv}$, and $I_{v,tot}^m$ is the tolerable interference such that $\gamma_v^\text{tar}$ can be met on RB$_m$.

2. Considering RSRPs of the neighbouring cells; as any reference signal is transmitted at a fixed power, an interfering MS$_i$ can calculate the path gain on RB$_m$,
, to the affected $\text{BS}_v$, and assuming channel reciprocity, estimate the interference it is causing. It then uses the $I_{\text{m,tol}}^v$ from the vulnerable MS to calculate the maximum power, $\tilde{P}_{\text{max},i}$, for MS $i$ as

$$\tilde{P}_{\text{max},i} = \frac{I_{\text{m,tol}}^v}{C_{v,i}}. \quad (12)$$

It is clear that $\tilde{P}_{\text{max},i}$ is directly proportional to the tolerable interference, $I_{\text{m,tol}}^v$ at MS $v$.

Given the power adaptation scheme and assuming channel reciprocity, MS $v$ should achieve the required SINR target on RB $m$. However, in a FDD system where fast fading is not reciprocal, an interference margin must be applied. Lastly, since $I_{\text{m,tol}}^v$ is not directly available at MS $v$, this needs to be signalled from BS $v$ to MS $i$ via existing backhaul infrastructures.

### 3.3. Priority bands

In [19], soft frequency reuse, where RBs are arranged into priority bands, is envisioned for LTE systems to facilitate interference protection. In this work, the available spectrum is split into different priority classes. RBs assigned high-priority status are allocated to those MSs that require interference protection, and hence do not need to scale their transmit power. Looking from the other perspective, strongly interfering MSs are allocated RBs with a low-priority status, such that the transmit powers on these RBs may be reduced to provide interference protection. A priority class reuse scheme is established which, due to the power reduction, is an adaptive form of softer frequency reuse [10].

Three bands of communication, termed high-priority, mid-priority, and low-priority, are defined. These bands are allocated orthogonally, such that if a RB is assigned high-priority status in one cell, the same RB is assigned mid-priority and low-priority status in the neighbouring cells. In this sense, a priority class reuse factor of three results, which is shown in Figures 2 and 3.

When excessive interference is caused, the owners of mid- and low-priority RBs in the neighbouring cells must reduce their transmit power. This boosts the SINR on both the high- and mid-priority RBs. The power reduction procedure for ULIP is performed as follows:

1. The $I_{\text{m,tol}}^v$ for the high-priority RBs are calculated from (11), and distributed to the neighbouring cells.
2. The transmit powers on mid-priority RBs are adjusted according to (12) based on the $\min_{v \in I_m} \{I_{\text{m,tol}}^v\}$ received from high-priority RBs in neighbouring cells.
3. The $I_{\text{m,tol}}^v$ for the mid-priority RBs (after power scaling has been performed) are calculated from (11) and distributed.
4. The transmit powers on low-priority RBs are adjusted based on $\min_{v \in I_m} \{I_{\text{m,tol}}^v\}$ received from both neighbouring high- and mid-priority RBs.

It is clear that $I_{\text{m,tol}}^v$ can be re-calculated in every time slot. However, to reduce the signaling burden on the network, these updates are only distributed when a sufficient difference, $\delta$, to the last sent $I_{\text{m,tol}}^v$ has been observed.

Furthermore, all high-priority RBs receive interference protection, and consequently gains in achievable throughput. This is facilitated by the MSs assigned low- and mid-priority RBs, which have reduced their transmit power. MSs allocated mid-priority RBs may also receive a throughput boost, as the MSs assigned low-priority RBs also take the mid-priority $I_{\text{m,tol}}^v$ into account. MSs allocated low-priority RBs however, exclusively sacrifice transmit power and, consequently, throughput. The allocation of users to these priority bands (i.e., the assignment of $x$-priority RBs to MSs) is discussed in Section 5.

![Figure 2 Allocation of priority bands in neighbouring cells $v$, $i$, and $j$. The allocation of high-, mid- and low-priority RBs are complementary in the cells.](image-url)
3.4. Practical implementation in LTE systems: an example

In order to implement the ULIP procedure, the interfering (i.e., low-priority) MS needs to be informed of the \( I_{m,tol} \) of its high-priority counterpart (in the neighbouring cell), to be able to then adjust its transmit power according to (12). This involves integrating the proposed ULIP technique within the network architecture. In abstract, the following procedure can be used to incorporate ULIP in the LTE network architecture:

1. The vulnerable BS\(_v\) calculates the \( I_{m,tol} \) for all (allocated) high-priority RBs in the cell using the received uplink desired signal strength \( S^m_v \).

2. The \( I_{m,tol} \) are sent to all neighbouring BSs over the X2 or (if no X2 connection is available) S1 interfaces (see Figure 4 for LTE architecture).

3. The neighbouring BS identifies and stores the minimum \( I_{m,tol} \) received on each particular RB\(_m\), including the cell-ID from which it came.

4. The neighbouring BS prepares a Data Radio Bearer (DRB) containing the \( \min_{v_r} \{I_{m,tol}\} \) found and the cell-ID \( \nu_r \) for each of the low-priority RBs.

5. The DRBs are sent with the Radio Resource Control (RRC) protocol via the Physical Downlink Shared
Channel (PDSCH) to each of the MSs allocated the low-priority RBs (see Figure 5 for protocol).

(6) MS\textsubscript{i} (allocated low-priority RB) estimates \(G_{v,i}^m\) from BS \(v\) with \(\min\{I_{v}^{m,\text{tol}}\}\) indicated in DRB, using RSRP measurements.

(7) MS\textsubscript{i} calculates \(\hat{p}_{\text{max},i}\) according to (12), and adjusts transmit power to provide interference protection in neighbouring cells.

The BS needs to inform the interfering MS\textsubscript{i} of the interference margin \(I_{v}^{m,\text{tol}}\) of MS\textsubscript{v} on high-priority RB\textsubscript{m} as calculated from (11). Thus, the transport of this information from BSs to the corresponding MSs must be defined using the LTE network architecture depicted in Figure 4.

The S1 interface connects the Serving Gateway (S-GW)/Mobility Management Entity (MME) with groups of neighbouring BSs. The MME processes the signalling between an MS and the core network (CN). Neighbouring BSs (i.e., within the groups connected by the S1 interface) are interconnected via the X2 interface, which carries control information regarding handover and interference coordination. The X2 interface is therefore highly suitable for ULIP related signalling.

In LTE, the RRC protocol is used to transfer common (i.e., applicable to all MSs) and dedicated (i.e., applicable to only a specific MS) non-access stratum (NAS) information [27]. The RRC protocol covers a number of functional areas, including the broadcasting of system information, RRC connection control, network controlled mobility procedures, and measurement configuration and reporting. The RRC connection control handles all procedures related to the establishment, modification and termination of an RRC connection, including, among others, the formation of DRBs, radio bearers carrying user data [27].

In Figure 5, the construction, translation, and transmission of such a DRB is shown. Here, the DRB is multiplexed with other Signalling Radio Bearers (SRBs) and DRBs to then be transmitted to MS\textsubscript{v}. Furthermore, the Downlink Shared Channel (DL-SCH) and, consequently, the PDSCH are used for transmission of \(\min\{I_{v}^{m,\text{tol}}\}\) and the cell-ID, meaning that no extra signalling on the control channels is required. Of course, the transmission of these DRBs in every subframe would be highly signalling-intensive, and hence is to be avoided. While the serving BS will continuously update the \(I_{v}^{m,\text{tol}}\) for all
high-priority RBs, it only transmits these updates to the neighbouring BSs when a significant change, δ, in \( P_{u}^{\text{tol}} \) in comparison to the last transmission (e.g., due to high mobility, call dropping, etc.) is achieved. This reduces the information transfer from the BSs to the MSs, and consequently lessens calculational intensity at the MSs.

Finally, knowledge of the cell-ID allows MS, to read the cell-specific reference signals of the neighbouring BS providing \( \min \left\{ I_{v}^{\text{tol}} \right\} \), which is necessary to carry out the RSRP measurements and estimate the channel gain between the MS and the vulnerable BS, \( C_{v,i}^{m} \). This, of course, is needed by the MS, to perform its power adaptation according to (12). The RSRP for a specific cell is defined as the linear average over the power contributions of the resource elements, within the considered measurement frequency bandwidth, which carry the cell-specific reference signals [28]. Using these measurements, the power reduction procedure can take place.

4. Performance analysis

Given the detailed description of the ULIP technique, the expected performance of a system employing this mechanism can be explored. There are multiple analysis techniques that deal with such problems, more specifically with system capacity analysis. In [29–31], a reverse link capacity analysis assuming non-cooperative BSs (similar to the design of practical cellular systems) is unfortunately shown to be a long-standing open problem in information theory, but has been solved when treating the interference as Gaussian noise [32]. Clearly, since in ULIP the interference incident on each RB is dependent on the interference tolerances of other-cell high-priority MSs allocated this RB, the interference is most certainly not Gaussian. Hence, such an analysis is infeasible for a system employing ULIP. In [29,33], the area spectral efficiency is introduced as a capacity measure that utilises stochastic geometry (statistical analysis of the positions and gains of MSs in the system) to estimate the expected capacity of a cellular network. Because in ULIP the users in a cell are split into three interdependent groups, such an analysis would be difficult as it is not always clear (by position) which MSs are assigned high-, mid-, or low-priority. Furthermore, in [33] the interference is estimated stochastically, and since in ULIP the interference is dependent on individual MS requirements, this analysis would be misguided.

On the other hand, optimisation techniques [11,34] can be utilised to provide global solutions that optimise an overall performance goal (e.g., energy/spectral efficiency). Furthermore, these offer an overall characterisation of the wireless system. In ULIP, however, the aim is not to maximise/minimise any objective, but rather to provide individual MSs with the necessary interference mitigation such that these can achieve their SINR/rate requirements. This is clearly not a system-wide goal, and hence such a description of a ULIP system is not applicable.

In general, the main difficulty that is not overcome (in the aforementioned methods) is the multitude of interdependencies on each RB over the network. The transmit powers on an RB are dependent on the signal qualities of the users allocated this RB in other cells in the network. Furthermore, these interdependencies are constantly adapting depending on the SINRs of the individual MSs in each cell. Hence, the stochastic interference modelling used in capacity analysis techniques cannot be utilised to model cellular ULIP. Therefore, a theoretical comparison to the state-of-the-art is performed to highlight the potential benefits of ULIP for OFDMA networks. And while transmit power control is standard for the reverse link in future systems, it has been shown that maximum power transmission is capacity-achieving [29], and thus this is compared to ULIP here. Analytical derivations for the energy efficiency and system capacity performance of ULIP are presented.

4.1. Energy efficiency in ULIP

In a system that employs ULIP, the transmit powers of low-priority MSs (MSs allocated low-priority RBs) are reduced so that interference to other cells is mitigated. Clearly, the throughput of the low-priority MSs is diminished relative to the reduction in transmit power. However, given a measure for energy efficiency, it can be shown that ULIP guarantees energy efficiency gains.

Given the metric for energy efficiency defined in (7):

\[
\beta_{u} = \frac{C_{u}}{P_{u}} = \frac{B_{u} \log_{2} (1 + \gamma_{u})}{P_{u}} \quad \text{[bits/T]},
\]

it will be shown that the energy efficiency of MS\(_{u}\) after ULIP is applied is always greater than in the benchmark, where all MSs transmit at maximum power. Here, the Shannon capacity is used for ease of derivability and without loss of generality; and the calculation is performed independent of RBs, also with no loss of generality. Essentially, it will be shown that

\[
\beta_{u}^\text{ULIP} \geq \beta_{u}^\text{BM} \quad \text{or} \quad \frac{\beta_{u}^\text{ULIP}}{\beta_{u}^\text{BM}} \geq 1. \quad (13)
\]

4.1.1. Derivation

The proof proceeds as follows

\[
\frac{\beta_{u}^\text{ULIP}}{\beta_{u}^\text{BM}} = \frac{B_{u} \log_{2} \left( 1 + \frac{P_{u}^\text{ULIP} G_{u}}{I + N} \right)}{B_{u} \log_{2} \left( 1 + \frac{P_{u}^\text{BM} G_{u}}{I + N} \right)} \leq \frac{p_{u}^\text{ULIP}}{p_{u}^\text{BM}}.
\]

\[
\frac{p_{u}^\text{ULIP}}{p_{u}^\text{BM}} = \frac{B_{u} \log_{2} \left( 1 + \frac{P_{u}^\text{ULIP} G_{u}}{I + N} \right)}{B_{u} \log_{2} \left( 1 + \frac{P_{u}^\text{BM} G_{u}}{I + N} \right)}.
\]
where $P_u^{BM}$ is the benchmark transmit power, and $P_u^{ULIP}$ the power when ULIP is applied

$$P_u^{ULIP} = \alpha P_u^{BM}, \quad 0 \leq \alpha \leq 1. \tag{18}$$

This is substituted into (14) to obtain (15)

$$\frac{\beta_u^{ULIP}}{\beta_u^{BM}} = \log_2 \left( 1 + \frac{\alpha P_u^{BM} G}{I + N} \right) \frac{P_u^{BM}}{\log_2 (1 + \alpha c)} \left( 1 + \frac{P_u^{BM} G}{I + N} \right) \alpha P_u^{BM},$$

$$= \frac{\log_2 (1 + \alpha c)}{\log_2 (1 + c)} \alpha,$$

where $c = \frac{P_u^{BM} G}{I + N}$. After rearranging (15) in the following manner

$$\log_2 (1 + \alpha c) \geq \log_2 (1 + c),$$

$$\log_2 (1 + \alpha c) \geq \log_2 (1 + c) = \log_2 (1 + c) \alpha.$$

The generalised Bernoulli’s inequality can be applied to prove the inequality in (17), which states

$$(1 + x)^r \leq 1 + rx, \quad r \in \mathbb{R}, \quad 0 \leq r \leq 1, \quad x \in \mathbb{R}, x > -1. \tag{19}$$

To apply this to (17), $r$ and $x$ are set to

$$r = \alpha, \quad 0 \leq \alpha \leq 1 \quad \rightarrow \quad 0 \leq r \leq 1,$$

$$x = c, \quad c \geq 0 \quad \rightarrow \quad x \geq 0 > -1,$$

and replaced in (18), such that

$$(1 + x)^r \leq 1 + rx,$$

$$(1 + c)^r \leq 1 + \alpha c,$$

exactly the inequality from (17). Hence, by proving (17), it has been shown that (13) is indeed true

$$\frac{\beta_u^{ULIP}}{\beta_u^{BM}} \geq 1, \quad \forall P_u^{BM} \geq P_u^{ULIP} \geq 0,$$

and hence it can be concluded that the energy efficiency of a low-priority MS employing ULIP is always greater than or equal to the energy efficiency of the same MS in the benchmark system (i.e., transmitting at maximum power). Furthermore, since MSs on high-priority RBs receive a capacity boost while maintaining transmit power, their energy efficiencies are also enhanced. Therefore, the energy efficiency of any/every MS in the system is augmented during ULIP operation, and consequently also the system energy efficiency

$$\beta_{sys}^{ULIP} \geq \beta_{sys}^{BM}. \tag{20}$$

For completeness, a similar proof can be constructed to show that in conjunction with a larger energy efficiency, the energy consumption $\psi_u = \frac{P_u G}{\gamma_u}$ measured in $\text{bit}$, for ULIP is lower (as expected) than for the benchmark. Essentially,

$$\frac{\psi_u^{ULIP}}{\psi_u^{BM}} \leq 1, \quad \text{and} \quad \psi_{sys}^{ULIP} \leq \psi_{sys}^{BM}. \tag{21}$$

### 4.2. System capacity in ULIP

It has been shown that through the application of ULIP the energy efficiency of not only the individual MSs but also of the system is always improved (at minimum no losses are incurred). However, due to the reduction in overall system power through ULIP, one would expect, in general, a similar decrease in system capacity. Here it will be shown that this is not always the case, and hence ULIP not only guarantees a energy efficiency boost, but can also provide a gain in system capacity.

$$C_{sys}^{ULIP} \geq C_{sys}^{BM}. \tag{22}$$

In essence, it is shown that (22) is true, which, combined with the energy efficiency results demonstrates the potential of ULIP for future OFDMA-based wireless networks such as LTE and/or LTE-Advanced. The proof is found in Appendix.

In the previous section it was demonstrated that the energy efficiency of any MS in a network will be enhanced when ULIP is employed, while here it has been shown that this energy efficiency boost can also be accompanied by an increase in the system capacity

$$C_{sys}^{ULIP} \geq C_{sys}^{BM}, \quad \beta_{sys}^{ULIP} \geq \beta_{sys}^{BM}. \tag{22}$$

Although in certain scenarios a loss in system capacity is incurred by the system-wide power reduction (as (22) suggests), the guaranteed energy efficiency gain can compensate this deficit. Furthermore, the possibility of gains in both performance metrics, i.e., when $C_{sys}$ is improved, is a good indication of the benefits ULIP can bring to future wireless networks.

### 5. Scheduling

To facilitate the interference protection, a scheduling procedure is designed to assign MSs to specific priority bands, enhancing the effect of ULIP in the system. In general, a random allocation of priority RBs can lead to undesired scenarios. For instance, the allocation of a high-priority RB to cell-centre MSs is wasteful, as such a MS-BS link is generally strong, and hence interference protection is unnecessary. At the cell-edge, allocating a low-priority RB to a MS is just as destructive. In this case, the MS will most probably be unable to sustain its
\( \gamma^{\text{avg}} \), and hence fall into outage. Therefore, an appropriate scheduling mechanism is necessary for ULIP to achieve its full potential.

In a fair allocation scheme, cell-edge MSs should be allocated high-priority RBs so as to be able to transmit at full power and achieve the maximum possible SINR. Cell-centre users, which are more likely to achieve their SINR target due to BS proximity, should be assigned low-priority RBs. In essence, the general rule is to allocate high-priority RBs to the MSs with the least favourable SINR conditions.

Therefore, an efficient scheduling procedure can increase the effectiveness of ULIP, and prevent throughput losses due to MS outages. In this section, a scheduling procedure relying on the reverse link signals of the active users is presented. By analysing the signals, an approximation of the relative positions of the MSs (and their interferers) can be obtained, which can then be used to schedule the users accordingly. This presents a low complexity scheduling solution, as the necessary information is readily available at the BS.

5.1. SINR scheduling

The scheduling procedure utilises the SINRs from transmissions in previous time slots. In (23), \( \mathcal{R}_j \) denotes the \( N_j \)-tuple of average (i.e., time average over the previous \( z \) time slots, where \( z \) is a system wide parameter) SINRs of the users in a cell

\[
\mathcal{R}_j = (\bar{\gamma}_{j1}, \bar{\gamma}_{j2}, \ldots, \bar{\gamma}_{jN_j}),
\]

where \( \bar{\gamma}_{ji} \) is the average SINR (over all assigned RBs) of MS \( i \) in cell \( j \), and \( N_j \) denotes the number of MSs in cell \( j \). The MSs that are at the cell-edge experience, on average, weaker signals, and consequently low SINRs are received at their serving BS. Thus, the next step is to sort the \( \bar{\gamma}_{ji} \) in ascending order, so that the MSs that have the weakest SINRs can be identified

\[
\mathcal{U}^*_j = \{ R_j \} = (p_1, p_2, \ldots, p_{N_j})
\]

s.t. if \( p_k \leq p_l \), then \( \bar{\gamma}_{jk} \leq \bar{\gamma}_{jl} \)

where \( \mathcal{U}^*_j \) is the \( N_j \)-tuple of the positions \( p_k \) of \( \bar{\gamma}_{jk} \) in the tuple \( \mathcal{R}_j = \text{order} (R_j) \), which is sorted in ascending order. The function \( f_j(\cdot) \) that defines this ordering can now be applied to the set of users in the cell of interest \( \mathcal{S}_{\text{users},j} \), and the set of high-priority MSs, \( \mathcal{S}_{hp,j} \), can be found

\[
\mathcal{S}_{hp,j} = \left\{ s \in \mathcal{S}_{\text{users},j} | f_j(\gamma_{js}) \geq \frac{N_j}{l} \right\}
\]

where \( \mathcal{S}_{hp,j} \subset \mathcal{S}_{\text{users},j} \)

where \( l \) denotes the number of priority bands such that the number of high-priority MSs yields \( \left\lceil \frac{N_j}{l} \right\rceil \). In (25), the high-priority RBs are allocated to the \( \left\lceil \frac{N_j}{l} \right\rceil \) MSs with the weakest average SINRs, and hence to the cell-edge. The low-priority RBs are allocated to the cell-centre, thus to the \( \left\lceil \frac{N_j}{l} \right\rceil \) MSs with the strongest SINRs, and the mid-priority RBs to the remaining (middle set) MSs:

\[
\mathcal{S}_{mp,j} = \left\{ s \in \mathcal{S}_{\text{users},j} | \frac{N_j}{3} \leq f_j(\gamma_{js}) \leq \frac{2N_j}{3} \right\}
\]

\[
\mathcal{S}_{lp,j} = \left\{ s \in \mathcal{S}_{\text{users},j} | f_j(\gamma_{js}) \geq \frac{2N_j}{3} \right\}
\]

where \( \mathcal{S}_{mp,j}, \mathcal{S}_{lp,j} \subset \mathcal{S}_{\text{users},j} \).

One instance of the fair allocation for exactly \( N_j = M = 50 \) users per cell is depicted in Figure 6.

It is clear to see that the farther MSs (from the serving BS) have been allocated high-priority RBs, and to the nearer MSs, which are shielded from neighbouring cell interference, the low-priority RBs are assigned. The mid-priority RBs have been assigned to the remaining MSs.

When a new MS enters the cell, the initial allocation is performed using the SNR (which can be approximated using the RSRP), as no SINR information is available a priori. Mean SINR statistics are employed to eliminate fast fading effects and prevent a MS from rapidly changing priority class, so that the system can reach a stable operating point.

![Figure 6 Allocation of resources using the fair scheduler: Each MS is depicted with a dot. The MSs marked with squares have been assigned high-priority RBs, triangles represent low-priority RBs, and the (unmarked) rest are mid-priority. The system is dubbed “fair” as high-priority is assigned to the MSs with the least favourable SINR conditions.](image-url)
6. Simulation
Monte Carlo simulations are used to provide performance statistics of the users and the system with and without ULIP. The simulator is built following LTE specifications.

6.1. Network construction and user distribution
The simulation area is comprised of a single-tier, tessellated hexagonal cell distribution. To eliminate border effects with regards to interference, an additional two tiers are simulated. However, statistics are only taken from the first tier (and centre cell). Users are distributed uniformly over the simulation area such that each cell hosts, on average, \( \bar{N}_j \) MSs. Further, BS-MS allocation is determined. The horizontal signal attenuation due to MS position is maximum possible attenuation \([24]\). Through (28), the horizontal azimuth antenna pattern, \( A(\theta) \), is described by

\[
A(\theta) = -\min\left\{12\left(\frac{\theta}{\theta_{3dB}}\right)^2, A_m\right\}
\]  

(28)

where \( \theta \) is the angle the MS-BS link deviates from the central lobe, \( \theta_{3dB} \) is the angle at which the gain is half that of at the centre of the lobe, and \( A_m \) is the maximum possible attenuation \([24]\). Through (28), the horizontal signal attenuation due to MS position is determined.

6.2. Resource allocation
The priority classes in each cell are organised in the manner portrayed in Figure 3, such that when a MS is allocated to a particular priority class, its RBs (if it is assigned more than one) can be allocated contiguously, a feature particular to an LTE uplink. The allotment of users to priority classes is performed by the SINR scheduler introduced in Section 5. Within each class, the set of RBs is randomly (but still contiguously) allocated to the MSs assigned to that class, with each user receiving at minimum one RB.

6.3. Time evolution
Each run of the Monte Carlo simulation is iterated over \( z = 10 \) subframes, or, equivalently, one LTE frame, such that long-term SINR statistics can be gathered. Due to the random user distribution, plentiful runs with different network generations are considered in order to obtain statistically accurate results. In each run, i.e., at the start of each subframe, the scheduling and allocation of RBs is reperformed. The MSs are assumed to be quasi-static for the duration of a run.

The simulation is performed for a full-buffer model, which represents the worst-case scenario where all users in the network are active, and no RB is left idle. Furthermore, the users are assumed to be static for the duration of a subframe, such that effects due to Doppler spread can be neglected. Perfect synchronisation in time and frequency is assumed, such that intra-cell interference is avoided. The relevant simulation parameters can be found in Table 2.

6.4. Benchmark
To evaluate the performance of ULIP, two well-known benchmark systems have been implemented for comparison purposes. These are:

- **Maximum power transmission**: In the first benchmark, no power allocation is performed, and all MSs transmit at the maximum power on each RB.
- **LTE power control**: In the second benchmark, the transmit power is set dependent on the nominal SINR target \( \Gamma \), the desired link path loss \( L_{\text{des}} \), the strongest interfering link loss \( L_{\text{int}} \), and the average interference received on that RB \( I_{\text{avg}} \). Here, LTE fractional power control (FPC) \([26]\) is used, where

\[
P_{\text{dim}} = \min\left\{\Gamma, \frac{P_{\text{avg}, \text{dim}}}{\Gamma}, \alpha L_{\text{des}, \text{dim}} + (1 - \alpha) I_{\text{int, \text{dim}}}, P_{\text{max, \text{dim}}}\right\}
\]

(29)

Table 2 Simulation parameters

| Parameter                  | Value     |
|----------------------------|-----------|
| Simulation area            | 37 cells  |
| Results area               | inner 7 cells |
| Inter-site distance, \( d_s \)  | 350 m  |
| Average MSs per cell, \( \bar{N}_j \) | 20      |
| Uplink FDD band            | [2.50, 2.51] GHz |
| Number of available RBs, \( M \) | 50      |
| RB bandwidth, \( B_{\text{RB}} \) | 180 kHz |
| Subcarriers per RB, \( k_{\text{sc}} \) | 12      |
| Symbol rate per subcarrier, \( g_{\text{sc}} \) | 15 ksps |
| Subframe duration, \( t_f \) | 1 ms    |
| Subframes (time slots), \( z \) | 10      |
| Thermal noise, \( \eta \)  | -174 dBm/Hz |
| Total MS transmit power    | 23 dBm   |
| Sector width               | 120°     |
| Sector \( \theta_{3dB} \)  | 70°      |
| MS SINR target, \( \Gamma_{\text{tar}} \) | 12 dB   |
| Standard deviation, \( \sigma \) | 4 dB    |
| Auto-correlation distance  | 50 m     |
which, depending on \( \alpha \), achieves a balance between conventional power control \( (\alpha = 1) \) and maximum power transmission \( (\alpha = 0) \).

For each of the benchmarks, the RB allocation from the ULIP system is adopted, resulting in a soft frequency reuse scheme \([36]\). By comparing the performance of ULIP to these two benchmarks, the effect ULIP has on the performance of the system can be quantified.

6.5. Results

The performance of the system is measured by three criteria: achievable throughput, energy efficiency and fairness (as defined in (5), (7), and (8), respectively). Multiple iterations are run for a system employing ULIP and the benchmark systems. The cumulative distribution functions (CDFs) of achievable throughput and energy efficiency of individual MSs and of the network are compared. From this, quantitative average gain/loss statistics are generated.

7. Results and discussion

From the simulation, the CDFs of the achieved system throughput and energy efficiency are generated for systems employing ULIP and compared against the two benchmark systems, keeping the RB allocation unchanged. General simulation parameters are taken from Table 2 and \([37]\), and full power control \( (i.e., \alpha = 1) \) is implemented.

In Figure 7, the CDFs of the achieved user throughput for the three systems is shown, and it is evident that ULIP achieves considerable gains for MSs with low throughput in the benchmarks. At the 50th percentile, ULIP users achieve, on average, \( 2.8 \times \) the user throughput of both benchmarks.

Also, although at the 90th percentile a 31% loss is incurred by the power reduction on low-priority (and therefore high-throughput) RBs, the crossing point of the CDFs signifies that 82% of the users achieve a better SINR (and consequently throughput) in ULIP. Furthermore, the \( \approx 20\% \) outage seen in both benchmarks is eliminated, and hence ULIP provides significant advantages for the users in a cellular network.

These benefits are further seen in Figure 8, where the user energy efficiencies of the three systems are displayed. Here it is clear that ULIP provides a vast energy

![Figure 7](image_url)
efficiency improvement over the two benchmarks, which
behave very similarly. At the 50th percentile, ULIP
induces almost $11\times$ the user energy efficiency of both
benchmarks.

Furthermore, ULIP achieves energy efficiency gains for
all MS over the maximum power benchmark, confirming
the result of the performance analysis conducted in
Section 4.1.

Figure 9 displays the system throughput fairness
results of the three power allocation techniques. Here, it
is clear to see that while power control provides some
fairness gains (almost 14%) over maximum power trans-
mission, ULIP achieves by far the fairest system with
over 0.8 fairness rating.

The substantial gains achieved by ULIP over maxi-
mum power transmission ($3.3\times$) can be accounted for
by the balancing of the system capacity from the cell-
centre to the cell-edge, boosting high-priority through-
put by sacrificing that of the low-priority MSs, and
hence achieving a more throughput fair system.

A further indicator of the enhanced fairness of the
network is shown in Figure 10, where the MS through-
put is plotted against the distance between the MS and
its serving BS. And while both the maximum power and
power control generate most of their capacity in the
cell-centre (MSs closer to the BS), ULIP achieves an
almost flat, much more even areal distribution of
throughput in each cell. These findings confirm both
the user throughput and fairness results shown in Fig-
ures 7 and 9, respectively. Furthermore, due to the
simulation environment, the gains for many MSs are
quite low, and hence power control very often utilises
maximum transmit power to attempt to achieve the tar-
get SINR. Hence, there is little performance difference
between the two systems, as is evident in Figure 10.

In Figure 11, the system throughput CDF results for
ULIP, power control and maximum power transmission
are shown. At the 50th percentile, it can be clearly seen
that while power control surrenders a slight portion ($\approx$
4%) of the system capacity achieved by maximum power
transmission, ULIP produces a gain of over 15%, resulting from the large number of MSs given throughput boosts (see Figure 7).

This is a very encouraging result, as it shows that the throughput shift from low- to high-priority MSs is beneficial for the system, achieving larger throughput gains for the high-priority users than losses by the low-priority MSs. This is also a direct result of the link adaptation, as any excess SINR (i.e., $\gamma > 20\, \text{dB}$) at the cell-centre can be transferred to the cell-edge without incurring any throughput losses for the low-priority (cell-centre) users. Furthermore, Figure 11 confirms the result achieved in Section 4.2, and shows further that system capacity gains are achievable.

In Figure 12, it can be seen that, surprisingly, power control exhibits an even worse energy efficiency than maximum power transmission. This is mainly due to the system throughput losses incurred. As expected, however, ULIP provides substantial gains over both benchmark systems, achieving a stout $3.5 \times$ and $3.6 \times$ the energy efficiency of max. power and power control at the 50th percentile, respectively. The large gains seen by ULIP are a combination of (a) the system throughput boosts achieved via the effective shifting of SINR from the cell-centre to the cell-edge; and (b) the substantial power reductions of the low- and mid-priority (cell-centre) users to protect the high-priority users from interference. Together, these two processes provide the significant energy efficiency gains seen in Figure 12, and confirm (20).

All in all, ULIP dominates each of the two benchmarks over the three performance criteria, especially providing a much more energy efficient and fair system. Furthermore, by achieving considerable gains in network capacity, it is clear that both performance analysis proofs have been confirmed.

8. Summary and conclusions
Full frequency reuse and the resulting large CCI in OFDMA networks brings forth the necessity for ICIC in future wireless networks. A technique for ULIP has been presented in this article, which provides protection from CCI through the power reduction of a subset of the neighbouring cell RBs, based on the SINR targets of the MSs in the cell of interest. Aside from the fact that no extra signalling is necessary over the control
channels, a further benefit of ULIP is a guaranteed increase in energy efficiency of all MSs in the system, and of the system as a whole. Furthermore, it was shown that while a loss in system capacity is possible, this is not certain, and hence gains in achievable system throughput are also possible. This is especially the case in networks where cell-edge capacity is limited, and most of the cell throughput is concentrated in the cell-centre.

It was shown that ULIP, combined with the SINR scheduler, achieves not only a 15% system capacity gain, but also substantially increases the system energy efficiency and fairness by 3.5× and 3.3×, respectively. This is a direct result of the SINR displacement from the cell-centre to the cell-edge, and confirms the results in Section 4, highlighting the excellent energy efficiency of the ULIP protocol. A throughput drop is seen when power control is applied, mainly due to the SINR targeting of the system in comparison to maximum power, which does not restrict transmit power according to service requirements. Furthermore, ULIP eliminates the ≈20% outage suffered in the benchmarks, and provides throughput gains for over 80% of the MSs in the network. Consequently, ULIP diminishes the tradeoff between system capacity and fairness/energy efficiency, and provides significant gains in all three performance areas.

**Endnotes**

aIn Table 1, the modulation and coding schemes are taken from LTE [27], and the SINR ranges from [38]. Here, the downlink values are used because no uplink implementation was found, as these values are operator specific. bThese denote the priority status of the RBs within each class, and have no relation to user traffic priorities, which are not considered here.

**Appendix**

**System capacity proof derivation**

To prove (22), a counter-argument to the assumption that

$$C_{\text{SYS}}^{\text{ULIP}} \leq C_{\text{SYS}}^{\text{BM}},$$

must be found, where $C_{\text{SYS}}$ is defined in (6). Therefore, a scenario is designed where the above assumption (30)
does not hold. A two-link scenario is chosen where MS1 and MS2 are allocated the same RBs in two neighbouring cells. Furthermore, we compare the $C_{\text{sys}}$ achieved in the benchmark (BM) system, in which all transmitting stations (MS1 and MS2) transmit using maximum transmit power, to that achieved in the ULIP system. When ULIP is applied, MS2 is given high-priority, and MS1 low-priority status such that it may be required to scale its power.

BM: $P_1 = P_2$
ULIP: $\alpha P_1 \leq P_2$, $0 \leq \alpha \leq 1$

where $\alpha$ is the scaling factor by which MS1 reduces its transmit power.

The proof is set up by making the assumption that the system is interference-limited, and hence the thermal noise can be ignored. This assumption depends on the inter-site distance $d_{\text{IS}}$ in the network, as clearly in larger cells the CCI diminishes (given $P_{\text{max}}$ remains constant). The path gain and path loss equations are given by (9) and (10), respectively, and the thermal noise is calculated to be $\eta = kTB_{\text{RB}} = -121$ dBm, where $k$ is Boltzmann’s constant, the temperature $T = 300$ K, and the bandwidth $B_{\text{RB}} = 180$ kHz per RB. Given that, on average, $|H_{k,l}|^2 = 1$ and $X_n = 0$, the minimum average interfering link gain can be calculated when the interfering MS is located at the maximum distance $d_{\text{max}} = d_{\text{IS}}$ from the vulnerable BS (i.e., next to a neighbouring BS):

$$L(d_{\text{max}}) = 15.3 + 37.6 \log_{10}(350) = 110.9 \text{ dB},$$  \hspace{1cm} (31)

$$G_{\text{min},v2} = \frac{-L(d)}{10} = -110.9 \text{ dB}.$$  \hspace{1cm} (32)

And given $P_u = P_{\text{max}}/M = 6$ dBm, the minimum received interference is $P_uG_{\text{min},v2} < -104.9$ dBm, which is significantly larger than $\eta$. In fact, even for $d_{\text{IS}} = 500$ m, the minimum average interference comes to -116.8 dBm, which is still more than double the noise power.

Hence, assuming the network is constructed with $d_{\text{IS}} < 500$ m, it has been shown that the system is interference-limited, and therefore the noise can be neglected.
This simplifies capacity calculations, as SIR can now be used rather than SINR. The individual user capacities are

\[ C_{BM}^{i} = W \log_2 \left( 1 + \frac{P_1 G_{1i}}{P_2 G_{2i}} \right) \]  

in the benchmark system, and

\[ C_{ULIP}^{i} = W \log_2 \left( 1 + \frac{\alpha P_1 G_{1i}}{P_2 G_{2i}} \right) \]  

when ULIP is employed, where Shannon’s equation is used for the calculations. Subsequently, the relationship between \( C_{BM}^{i} \) and \( C_{ULIP}^{i} \) is found:

\[ C_{ULIP}^{i} \geq C_{BM}^{i} \]  

and finally, \( C_{BM}^{1} \) and \( C_{BM}^{2} \) are substituted into (36) to achieve (37)

\[ C_{ULIP}^{1} \geq \frac{1}{\alpha} C_{BM}^{1}, \quad C_{ULIP}^{2} \geq \frac{1}{\alpha} C_{BM}^{2}. \]  

For further simplicity, let us assume that \( G_{11} = G_{22}, \) and \( G_{12} = G_{21} \) (e.g., both MSs are at the cell-border). This creates the following set of equations:

\[ C_{BM}^{1} = C_{BM}^{2} = C_{i}^{BM}, \quad C_{ULIP}^{1} \geq \frac{1}{\alpha} C_{BM}^{1}, \quad C_{ULIP}^{2} \geq \frac{1}{\alpha} C_{BM}^{2}. \]  

Using (38), it can now be shown that the assumption in (30) does not hold for this system, and that hence (22) is true. In the benchmark,

\[ C_{sys}^{BM} = C_{1}^{BM} + C_{2}^{BM} = 2C_{i}^{BM}. \]  

And when ULIP is applied,

\[ C_{sys}^{ULIP} = C_{1}^{ULIP} + C_{2}^{ULIP}. \]  

Figure 12: System energy efficiency performance
where in (40), the equations from (38) are substituted into (39), and in (41), the inequality
\[
\left( \frac{\alpha + 1}{\alpha} \right) \geq 2
\]
is used, which is proven by the inequality of arithmetic and geometric means
\[
\frac{a + b}{2} \geq \sqrt{ab},
\]
\[
a = \alpha, \quad b = \frac{1}{\alpha}, \quad \left( \frac{\alpha + 1}{\alpha} \right) \geq 2 \sqrt{\frac{1}{\alpha}} \geq 2.
\]

In (39)-(41) it has been demonstrated that for the chosen scenario, the ULIP system capacity is greater than that of the benchmark system
\[
C_{ULIP} \geq C_{BM},
\]
and that, hence, (30) is not true. Therefore, (22) is valid.
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