Strong pressure dependence of the magnetic penetration depth in single crystals of the heavy fermion superconductor CeCoIn$_5$ studied by muon spin rotation

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In the tetragonal heavy ferrointrum system CeCoIn$_5$, the unconventional superconducting state is probed by means of muon spin rotation. The pressure dependence ($0 - 1$ GPa) of the basal-plane magnetic penetration depth ($\lambda_\parallel$), the penetration depth anisotropy ($\gamma = \lambda_\parallel/\lambda_\perp$) and the temperature dependence of $1/\lambda_i^2$ ($i = a, c$) were studied in single crystals. A strong decrease of $\lambda_\parallel$ with pressure was observed, while $\gamma$ and $\lambda_i^2(0)/\lambda_i^2(T)$ are pressure independent. A linear relationship between $1/\lambda_\parallel^2(270$ mK) and $T_c$ was also found. The large decrease of $\lambda_\parallel$ with pressure is the signature of an increase of the number of superconducting quasiparticles by a factor of about 2.

Unconventional superconductors are characterized by their proximity to different instabilities. In heavy fermion systems superconductivity is often found in the region of the phase diagram where a weak magnetic phase disappears [1]. However, in some systems [2] superconductivity is also detected in proximity of a valence phase transition.

CeCoIn$_5$ is a prototypical heavy fermion superconductor [3] at the focus of numerous studies owing to the proximity of quantum criticality. This proximity is reflected by the pronounced non-Fermi liquid features [4] and the highest superconducting (SC) transition temperature $T_c = 2.3$ K [3] among the Ce-based heavy fermions. In addition, this tetragonal system is characterized by a quasi-two-dimensional Fermi surface [5, 6] and a two-gap unconventional SC state with d-wave symmetry [6, 7].

In order to clarify the relation between the SC phase and quantum criticality, the evolution of basic SC parameters with respect to a tuning parameter is required. In this letter the pressure ($p$) and temperature ($T$) dependence of a fundamental SC quantity — the magnetic penetration depth ($\lambda_i$) — was studied. Here $i = a, c$ corresponds to a screening current flowing along the main crystallographic directions: perpendicular, respectively parallel to the c-axis. $\lambda_i$ is obtained through the precise magnetic field distribution in the SC vortex state probed by transverse-field (TF) muon-spin rotation ($\mu$SR).

CeCoIn$_5$ is in the clean limit with a ratio of coherence length to mean free path $\xi/l < 0.02$ ($\xi < 8.2$ nm) [5, 7]. In this limit the penetration depth can be written in the London model as:

$$1/\lambda_i^2 = \mu_0 e^2 n_S/m_\ast^i$$  \hspace{1cm} (1)

Here $\mu_0$ is the vacuum permeability, $e$ the electron charge, $n_S$ the number density (number of superconducting quasiparticles), and $m_\ast^i$ the effective quasiparticle mass.

The $\mu$SR experiments were performed at the Swiss Muon Source (S$\mu$S), Paul Scherrer Institute (PSI), Switzerland, using the GPD (under $p$) and LTF (ambient $p$, low $T$) spectrometers. In a TF-$\mu$SR experiment spin polarized positive muons are implanted into a sample in an external magnetic field $\mu_0 H$ (field cooled above $T_c$) applied perpendicular to the initial muon-spin polarization. In the presence of a magnetic field at the muon site $B_\mu$ the muon spin precesses at its Larmor frequency $\omega_\mu = \gamma_\mu B_\mu$ ($\gamma_\mu = 8.516 \cdot 10^6$ rad s$^{-1}$T$^{-1}$) is the gyromagnetic ratio of the muon) before decaying with a life time of $\tau_\mu = 2.2$ $\mu$s into a positron and two neutrinos. Due to parity violation the decay positron is preferentially emitted along the muon spin direction. Forward and backward positron detectors with respect to the initial muon polarization are used to monitor the $\mu$SR asymmetry spectrum $A(t)$.

Single crystals of CeCoIn$_5$ were grown by indium flux method [9] (rare earth from [10]), centrifuged and etched in HCl solution to remove the indium excess. Thin plate-like single crystals were obtained with their large faces corresponding to the (001) basal plane. Using this particular geometry, two samples were prepared, consisting of $\sim 10$, respectively $\sim 200$ crystals glued together with G.E. varnish, as sketched in Fig. 2 The mosaic sample ($c$-axis normal to the plane) was studied with the LTF spectrometer. The cylindrical-like sample ($a$-axis is the main axis) was mounted in a piston cylinder pressure cell of CuBe alloy with Daphne oil as a pressure transmission medium [11] and measured with the GPD spectrometer. The actual pressure in the cell was determined by the $T_c$ of a small piece of indium.

For different pressures an angular scan consisting of 5-8 TF-$\mu$SR spectra was taken at $T \approx 270$ mK with an
applied field $\mu_0 H \approx 50 \text{ mT}$ forming an angle $\theta$ with the sample’s crystallographic $c$-axis. For $p = 0 \text{ GPa}, 0.2 \text{ GPa},$ and $0.6 \text{ GPa}$ a temperature scan was also recorded for $\theta = 0^\circ (H \parallel c)$ and $\theta = 90^\circ (H \perp c)$, and the field was chosen to be higher than the critical field of bulk indium ($\mu_0 H_{c2}(0) = 23 \text{ mT}$) to avoid artifacts due to possible residual flux from the growth. For comparison the values of the Pauli limited critical fields for CeCoIn$_5$ are: $\mu_0 H_{c1} \approx 10 \text{ mT} (H \parallel c$ and $H \perp c)$, $\mu_0 H_{c2} = 5 \text{ T} (H \parallel c)$ and $11.5 \text{ T} (H \parallel c)$ \cite{6}. A field of $\mu_0 H = 50 \text{ mT}$ is also small enough so that the Knight shift \cite{7} and Zeeman current \cite{8} effects can be neglected in the analysis of the spectra. In the normal state about $6 \cdot 10^6$ and in the SC state $10 - 20 \cdot 10^6$ positrons events were recorded for a $\mu$SR time spectrum.

Typical TF-$\mu$SR time spectra in the normal and SC state are displayed in Fig. 1. The temporal oscillations and damping of the $\mu$SR asymmetry reflect directly the local magnetic field distribution at the muon stopping sites. The $\mu$SR time spectrum consists of two contributions: a background signal ($B_B$) arising from the muons stopping in the silver sample holder for the LTF spectrometer or the pressure cell for the GPD spectrometer and a signal arising from the muons stopping in the sample ($S$) \cite{4}. These contributions are clearly seen in Fig. 1. At short times the sample contribution dominates: in the SC state the damping of the signal is enhanced due to the field broadening generated by the vortex lattice (VL), and the oscillating frequency is reduced due to diamagnetic screening. In contrary, for $t > 7 \mu s$ in the normal state and $t > 3.5 \mu s$ in the SC state, only the signal of the muons stopping in the silver background persists. The $\mu$SR time spectra are well described with the following equation:

$$A(t) = A_0 [(1 - f_S(\theta))R_{B_B}(t) + f_S(\theta)R_{S}(t)]$$

Here $f_S(\theta)$ denotes the fraction of muons stopping in the sample, $A_0$ the initial asymmetry of the signal and $R_{S}(t)$ [$R_{B_B}(t)$] is the sample [background] muon depolarization function. $f_S(\theta)$ was determined to be $\approx 82\%$ for the LTF spectrometer and typically $\approx 45\%$ for the GPD spectrometer. Here $f_S(\theta)$ varies each time the pressure cell is manipulated (change of $p$ or $\theta$) as the sample position relative to the muon beam is modified. In various configurations we recorded a $\mu$SR spectrum after a small field increase of $4 \text{ mT}$ at low temperatures. Due to pinning the shift of field in the sample is less, allowing to determine precisely the fraction of muons stopping in the sample. The background depolarization function is described by a Gaussian field distribution \cite{11}:

$$R_{B_B}(t) = \cos(\gamma_\mu (B_{B_B}(\theta, T)t + \phi_0) \exp(-\gamma_\mu^2 \sigma_{B_B}^2(\theta, T)t^2/2)$$

The average background magnetic field $\langle B_{B_B}(\theta, T) \rangle \approx 50 \text{ mT}$ and the standard deviation of the Gaussian field distribution $\sigma_{B_B}(\theta, T)$ vary in the SC state since the diamagnetic sample induces a field inhomogeneity in its surrounding. The initial phase $\phi_0$ is constant.

The sample depolarization function may be written as:

$$R_{S}(t) = \exp(-\gamma_\mu^2 \sigma_{S}^2(\theta, T)t^2/2) \times \int P_{V_L}(B_0, T) \cos(\gamma_\mu B_0 t + \phi_0) dB_0$$

The presence of a VL gives rise to a local magnetic field distribution along the direction of the applied field.
$P_{VL}(B_0, T)$, reflected by the integral in Eq. (4). For an extreme type-II superconductor in the London limit $P_{VL}(B_0, T)$ is uniquely determined by an effective penetration depth $\lambda_{eff}(\theta, T)$ \[14\] \[15\]. For the two principal magnetic field orientations one has: $\lambda_{eff}(\theta = 0^\circ, T) = \lambda_a(T)$ and $\lambda_{eff}(\theta = 90^\circ, T) = \sqrt{\lambda_a(T)\lambda_b(T)}$. The first factor in Eq. (4) describes the muon depolarization due to additional contributions ($\sigma_{\perp}^2(\theta, T) = \sigma_{\parallel}^2(\theta) + \sigma_{VL}^2(\theta)$) \[16\]: (i) the nuclear moments $\sigma_N(\theta) \approx 0.5 \text{ mT}$ and (ii) the disorder of the VL $\sigma_{VL}^2(\theta, T) = (\sigma_{VL0}(\theta)\lambda_{eff}^2(\theta, 0)/\lambda_{eff}^2(\theta, T)$ with $\sigma_{VL0}(\theta) \approx 0.5 \text{ mT}$ \[17\]. The local magnetic field distribution in the sample $P_S(B_0, T)$ can be obtained from the cosine Fourier transformation (FT) of the experimentally measured $A(t)$, after subtraction of $R_{BG}(t)$ (Fig. 2).

The angular dependent spectra were analyzed globally [Eqs. (2) to (3)] \[18\] with the constraint that $\lambda_{eff}(\theta, T) = \lambda_a(T)\sqrt{\cos^2(\theta) + \gamma(T)\sin^2(\theta)}$ with $\gamma(T) = \lambda_a(T)/\lambda_a(T)$ \[19\]. $\lambda_{eff}(\theta, T = 270 \text{ mK})$ was used to determine the exact orientation of the sample in the pressure cell (position of $\theta = 0^\circ$). The pressure dependence of the obtained parameters $\lambda_a$ and $\gamma$ are shown in Fig. 3 (red circles). The analysis of the temperature dependent spectra treated globally \[18\] is also presented (black squares). The two data sets give similar results, although different assumptions were made ($T$ or $\theta$ dependence of some parameters fixed), demonstrating the reliability of the model.

The analysis yields at ambient pressure a value of $\lambda_a(T \to 0 \text{K}, \mu_0 H = 50 \text{ mT}) = 350(12) \text{ nm}$. Since in the London model the contribution of the vortex core is neglected, this value is overestimated \[20\]. Taking $\mu_0 H_{c2, orb} \approx 7.5 \text{ T}$ for the orbital upper critical field \[21\], this correction is only $\approx 4\%$ for an applied field of $\mu_0 H = 50 \text{ mT}$ and therefore was neglected. In comparison, the first $\mu$SR experiment reported $\lambda_a(0) \approx 550 \text{ nm}$ \[22\]. This experiment was performed in a large magnetic field $\mu_0 H = 0.3 \text{ T}$, and in the analysis an additional field broadening was neglected \[16\]. This is very likely the main reason for the larger value of $\lambda_a(0)$. Neutron diffraction experiments reported $\lambda_a(0)$ between 247(10) nm \[23\] and $\approx 465 \text{ nm}$ \[24\]. The first value, measured in a magnetic field of 2 T, was underestimated because Zeeman currents that produce an additional contribution to the field broadening \[25\] were neglected. The second value was deduced from measurements at 0.5 T. Including the correction for the vortex cores \[20\], we obtain $\lambda_a(0) \approx 360 \text{ nm}$ in agreement with the present value. Surface impedance techniques provided smaller $\lambda_a(0) \approx 260 \text{ nm}$ \[26\] and $\lambda_a(0) = 281(14) \text{ nm}$ \[27\]. These experiments were performed in an extremely low magnetic field ($\lesssim 10 \mu\text{T}$) in the Meissner state.

The temperature dependence of $\lambda_a^2(0)/\lambda_a^2(T)$ ($i = a, c$) is displayed in Fig. 4 together with a fit of the form $1 - (T/T_e)^n$. The pressure evolution of $T_e$ was determined independently by SQUID magnetometry (Fig. 5). The exponent $n$ was found to be $n = 2.17(6)$ for $i = a$ in agreement with Ref. \[28\], while $n = 1.35(19)$ for $i = c$. Similar temperature dependences can be obtained using $\Delta \lambda_i = \lambda_i(T) - \lambda_i(0)$ measured by tunnel-diode oscillator experiments \[20\] taking $\lambda_a(0) \approx 336 \text{ nm}$ and $\lambda_c(0) \approx 421 \text{ nm}$ from this work (green empty circles in Fig. 4). Within precision both $\lambda_a^2(0)/\lambda_a^2(T)$ ($i = a, c$) are pressure independent, suggesting that the gap symmetry is unchanged, and the value of the gap to $T_e$ ratio is constant, in agreement with the variation of less than 10% obtained by NQR \[29\] in this pressure range.

The pressure independent value of $\gamma = \sqrt{m_e^2/m_n^2} \approx 1.3$
The same experiments indicate that the variation cannot explain the pressure dependence of $1/\lambda^2_a(270 \text{ mK})$ in CeCoIn$_5$ with a maximum around 0.5 GPa. Such a small London model [Eq. (1)], plotted in Fig. 5. Therefore, we conclude that, within the London model, $n_S$ increases with pressure. Using an average value $m^*_S \approx 50 m_0$ [31] one obtains from Eq. (1) a change of $n_S$ from $n_S \approx 1.8$ to 3.4 carriers per unit cell between 0 and 1 GPa.

In the following we discuss two possible scenarios for this strong increase of $n_S$. The first one relies on the proposed multigap SC state of CeCoIn$_5$. The observed increase of $n_S$ with pressure would result from an increase of the small gap at 50 mT. Indeed, at ambient pressure for $\mu_0 H \approx 50 \text{ mT}$ the smaller gap is already closed [31]. To check whether the small gap could open under pressure, we probed the field dependence of the total magnetic field standard deviation in the sample. Here $\sigma^2_D = \sigma^2_S + (0.06092\Phi_0/\lambda^2)^2$ [14] is the quadratic sum of $\sigma_S$ previously defined and the magnetic field standard deviation generated by the VL (\(\Phi_0\) is the flux quantum). For comparison, for the two-gap superconductor PrOs$_4$Sb$_{12}$ [31] different slopes $d\sigma_D/dH$ are observed between the low magnetic field regime with two opened SC gaps and the high magnetic field regime where only one SC gap is present [32]. In CeCoIn$_5$, the fact that the magnetic field dependence of $\sigma_D$ is the same at 0 GPa and 0.6 GPa (inset Fig. 4), strongly suggests that a single gap is probed in the full pressure range.

Another scenario is based on an increase of the Ce valence (orbital occupancy $n_{v-a} \approx 0.9$ [33] at ambient pressure). Such a scenario was proposed for the parent compound CeRhIn$_5$ where a similar decrease of $\lambda_a$ is observed between $p = 2.07$ GPa and $p = 2.26$ GPa [34]. Note that valence fluctuations are often associated with SC in Ce based heavy fermions [33].

An interesting observation is the linear relation $T_c(\lambda_a) = T_{c0} + A/\lambda_a^2(270 \text{ mK})$ shown in Fig. 6. This relation has some analogy with the Uemura plot [36] found for underdoped cuprate superconductors and other electronically doped unconventional superconductors. However, substantial differences exist: (i) no proportionality ($T_{c0} \neq 0$) and (ii) $A$ is about 90 times smaller than $A_U$. In addition, pressure affects $1/\lambda^2_a$ much more in CeCoIn$_5$ than in cuprates [11].

In conclusion, we show by TF-\(\mu\)SR that in CeCoIn$_5$ the magnetic penetration depth ($\lambda_a$) decreases under pressure, while the anisotropy ($\gamma = \lambda_a/\lambda^*_a$) and the temperature dependence of the penetration depth ratios $\lambda^*_a(0)/\lambda^*_a(T)$ and $\lambda^*_a(0)/\lambda^*_a(T)$ are almost unaffected. In the range of pressure investigated, a linear dependence between $T_c$ and $1/\lambda^2_a$ was found. Within the London model, the decrease of $\lambda_a(270 \text{ mK})$ under pressure corresponds to a doubling of the number density ($n_S$) between 0 and 1 GPa, possibly related with the presence of a quantum critical point.

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