Magnetic structure of the Eu$^{2+}$ moments in superconducting EuFe$_2$(As$_{1−x}$P$_x$)$_2$ with $x = 0.19$

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(Received 26 May 2014; revised manuscript received 29 August 2014; published 9 September 2014)

The magnetic structure of the Eu$^{2+}$ moments in the superconducting EuFe$_2$(As$_{1−x}$P$_x$)$_2$ sample with $x = 0.19$ has been determined using neutron scattering. We conclude that the Eu$^{2+}$ moments are aligned along the $c$ direction below $T_C = 19.0(1)$ K with an ordered moment of $6.6(2) \mu_B$ in the superconducting state. An impurity phase similar to the underdoped phase exists within the bulk sample which orders antiferromagnetically below $T_N = 17.0(2)$ K. We found no indication of iron magnetic order, nor any incommensurate magnetic order of the Eu$^{2+}$ moments in the sample.

DOI: 10.1103/PhysRevB.90.094407 PACS number(s): 74.70.Xa, 75.25.–j, 75.40.Cx

I. INTRODUCTION

In the last few years, there has been a flurry of research activity in the field of unconventional high-$T_C$ superconductors [1] due to the discovery of iron-based superconductors in 2008 [2]. Among various classes of Fe-based superconductors [2–7], the ternary “122” system, AFe$_2$As$_2$ (A = Ba, Ca, or Sr, etc.) with $T_C$ up to 38 K [8–10], has been the most widely studied member of Fe-pnictide superconductors. EuFe$_2$As$_2$ is an interesting member of the “122” family since the A site is occupied by the Eu$^{2+}$, which is an S-state rare-earth ion possessing a 4f$^7$ electronic configuration with the electron spin $S = 7/2$ [11]. EuFe$_2$As$_2$ exhibits a spin-density wave (SDW) transition in the Fe sublattice concomitant with a structural phase transition at 190 K. In addition, Eu$^{2+}$ moments order in an A-type antiferromagnetic (AFM) structure at 19 K (ferromagnetic layers ordered antiferromagnetically along the $c$ direction) [12–14]. Superconductivity can be achieved in this system by substituting Eu with K or Na [9,15], As with P [16], and upon application of external pressure [17–19]. Doping as well as external pressure lead to a decrease of both the structural and Fe magnetic phase transition temperatures and eventually superconductivity appears when both transitions are suppressed enough [9]. Upon P doping, the ordering temperature of the Eu$^{2+}$ moments initially decreases by a few Kelvin until the superconductivity appears and then increases up to 30 K as the doping is increased further [20].

The superconducting dome for the P-doped EuFe$_2$As$_2$ is quite narrow compared to the other Fe-based “122” pnictides [21]. It is generally accepted that the Eu$^{2+}$ moments order antiferromagnetically before the superconducting dome and ferromagnetically after the superconductivity is suppressed [20]. However, the exact nature of the Eu$^{2+}$ magnetic order within the superconducting dome has remained controversial [22]. Most surprising is the coexistence of ferromagnetism and superconductivity, as recently proposed by many groups for the P-doped EuFe$_2$As$_2$ samples [22–26]. In particular, Zapf et al. [22,26] concluded, based on macroscopic measurements, that the Eu$^{2+}$ moments in EuFe$_2$(As$_{1−x}$P$_x$)$_2$ order in a canted A-type antiferromagnetic structure, with the spin component along the $c$ direction being ferromagnetically aligned. Zapf et al. [22] also discovered that the A-type antiferromagnetic order of the Eu$^{2+}$ moments below around 20 K undergoes a spin-glass transition at lower temperatures where the in-plane components of the magnetic moments are responsible for the glassy freezing. For the superconducting EuFe$_2$(As$_{1−x}$P$_x$)$_2$ samples with $x = 0.15$, we have recently concluded that the Eu$^{2+}$ moments are primarily aligned ferromagnetically along the $c$ direction using x-ray resonant magnetic scattering [27]. However, due to the limited sensitivity of the x-ray scattering technique for the ferromagnetic structures, the moment size could not be determined from the previous studies. Neutron-diffraction studies on a superconducting Eu(Fe$_{0.82}$Co$_{0.18}$)$_2$As$_2$ single crystal revealed a long-range ferromagnetic order of the Eu$^{2+}$ moments along the $c$ direction [28]. Due to the strong neutron absorption of the natural Eu (~5800 barns at $\lambda = 2.513$ Å) together with the small sample mass (~10 mg) of the P-doped single crystals compared to the Co-doped EuFe$_2$As$_2$ (~100 mg), the magnetic structure determination in EuFe$_2$(As$_{1−x}$P$_x$)$_2$ via neutron diffraction is considerably more challenging. The only attempt was made on a powder sample of the nonsuperconducting end member EuFe$_2$P$_2$, where it was concluded that the Eu$^{2+}$ moments order ferromagnetically with a canted angle of 17° from the $c$ axis [29]. Based on Mössbauer studies on superconducting polycrystalline samples, Nowik et al. [25] also concluded that the Eu$^{2+}$...
moments are aligned ferromagnetically along the c axis with a possible tilting angle of 20° from the c axis for EuFe$_2$(As$_{1−x}$P$_x$)$_2$ with $x \geq 0.2$. On the other hand, it was concluded for the Co-doped EuFe$_2$As$_2$ samples that the canting angle is nearly zero [28]. Therefore, it is very important to clarify the moment direction and the absolute value of the ordered moment using neutron diffraction for the P-doped EuFe$_2$As$_2$ single crystals with different doping levels. Here we report on the neutron-scattering studies of the superconducting EuFe$_2$(As$_{1−x}$P$_x$)$_2$ single crystal with $x = 0.19$ to explore the details of the magnetic structure of the Eu$^{2+}$ moments. Our neutron-scattering experiments show that the Eu$^{2+}$ moments order ferromagnetically along the c direction with an ordered moment of 6.6(2) $\mu_B$. No magnetic order associated with Fe or structural phase transition could be detected.

II. EXPERIMENTAL DETAILS

Single crystals of EuFe$_2$(As$_{1−x}$P$_x$)$_2$ with $x = 0.19$ were grown using FeAs flux [20]. For the scattering measurements, a 10 mg as-grown triangular-shaped single crystal of approximate dimensions $2.9 \times 3.5 \times 3.8$ mm$^3$ and thickness of 0.3 mm was selected (see inset of Fig. 1) and its phosphorous content was determined within 1% accuracy on four different spots by freshly cleaving the sample using EDX (energy dispersive x-ray analysis). High-resolution elastic neutron-scattering experiments were carried out on the cold-neutron triple-axis spectrometer IN12 at the high-flux reactor of the Institut Laue Langevin (ILL) in Grenoble, France. A vertically focused pyrolytic graphite (PG) (0 0 2) monochromator and analyzer were used. In addition, the monochromator was partially focused horizontally to optimize flux for the used collimators. In order to get the best scattering plane for measurements $\{1 1 0\}$, the sample was remounted after each measurement. The single crystal was mounted on a vanadium pin using a very small amount of GE-Varnish and mounted inside the ILL Orange-type cryostat. Furthermore, the sample stick near the sample as well as the vanadium pin were covered with a thick Cd foil for the reduction of background. Slits before and after the sample were used to further reduce the background. Initially measurements were performed in the $(1 0 0)$ scattering plane. Later, the sample was remounted in the $(1 0 0)$ scattering plane for measurements of more magnetic and nuclear reflections. Measurements at IN12 were performed at temperatures between 2 and 100 K. For convenience, we will use tetragonal (T) notation unless otherwise specified.

III. EXPERIMENTAL RESULTS

A. Macroscopic characterizations

Figure 1 shows the temperature dependence of the magnetic susceptibility $M/H$ measured for magnetic field parallel to the $a$-$b$ plane using a Quantum Design superconducting quantum interference device (SQUID) magnetometer. Zero-field cooled magnetization becomes negative at $T_{SC} = 27$ K, signifying a superconducting transition at this temperature. At slightly lower temperature and at $T_C = 19$ K, the superconducting signal is weakened by the onset of the Eu$^{2+}$ magnetic order and has been observed in heat-capacity measurements [20]. The transition at $T_C$ is the ferromagnetic transition of Eu$^{2+}$ moments as supported by the saturation of magnetization (FC susceptibility) as well as strong increase of the intensity for the nuclear reflections (see next section) below this temperature. Furthermore, it was found that the entropy release associated with this transition is close to the theoretical value of $R \ln(2S + 1)$ for the Eu$^{2+}$ moments with spin $S = 7/2$ on similar chemical compositions [20,27]. Superconductivity wins over the Eu$^{2+}$ magnetism if temperature is lowered further. The results of magnetic susceptibility are consistent with the published results of Jeevan et al. [20].

B. Neutron diffraction

It has been established for the parent compound as well as for the 15% P-doped samples that there is a structural phase transition from space group $14/mmm$ to $Fmmm$, with a distortion along the $[1 1 0]$ direction at 190 and 49 K, respectively [13,27]. To determine whether there is a similar structural phase transition, ($\xi \, \xi \, 0$) scans were performed through the tetragonal $(2 2 0)$ Bragg reflection as a function of...
temperature. Figure 2(a) shows the temperature dependence of the integrated intensity for the (2 2 0) reflection as the sample was warmed up from 2 to 70 K. It can be seen that there is an increase of intensity below \( T_{\text{c}} \approx 19 \text{ K} \), coincident with the onset of the magnetic order of the Eu\(^{2+}\) moments. No change in intensity at higher temperatures associated with the extinction release [28] at the structural phase transition has been observed. Figure 2(b) shows the temperature dependence of the full width at half maximum (FWHM) for the same reflection. However, the FWHM remains constant within the experimental error in the investigated temperature range [27].

For the undoped parent compound, the Fe moments order magnetically below 190 K with a propagation vector \( \tau = (1/2 \ 1/2 \ 1) \) [13]. Figure 2(c) shows \( \omega \) scans (rocking curves) through the expected position of the strongest magnetic peak at (1/2 1/2 3) at 25 K and at the background position of (1/2 1/2 2.7). Similar scans were performed at 2 K and 40 K (not shown). However, we failed to observe any magnetic peak corresponding to the Fe magnetic order, indicating the absence of the Fe magnetic order within our experimental accuracy.

For the parent compound, Eu\(^{2+}\) moments adopt an A-type antiferromagnetic structure characterized by the propagation vector \( \tau = (0 \ 0 \ 1) \). Figure 3 shows Q scans along the [0 0 1] direction at \( T = 2 \) and 25 K, respectively. For the (0 0 1) reflection, measurement has been performed only at 2 K due to the technical difficulties. The break in measurement data between \( L = 1.1 \) and 1.75 is due to the same difficulties. The temperature-independent peak near \( L = 5.04 \) is due to aluminum (Al). The peak positions near the (0 0 \( L \)) with \( L = \text{odd} \) were determined after fitting the peaks using Gaussian profiles.

FIG. 2. (Color online) (a) Temperature dependence of the integrated intensity for the (2 2 0) reflection. (b) Temperature dependence of the full width at half maximum (FWHM) for the same reflection. (c) Rocking scans at the expected position of the Fe magnetic order at (1/2 1/2 3) at 25 K and at the background position of (1/2 1/2 2.7).
fraction only 1.5%; see next section) together with the close proximity of the lattice parameters with the main phase.

Maps in the \((H H L)\) and \((H 0 L)\) planes were performed at \(T = 2\) K to search for additional magnetic peaks. Figures 4(a) shows a two-dimensional contour map around the very weak nuclear peak \((1 1 0)\). Only the main nuclear peak was observed, however, with intensity comparable to the strongest nuclear peaks. A similar contour map around another weak nuclear peak \((1 0 1)\) in the \((H 0 L)\) plane was performed and is shown in Fig. 4(b). In addition to the nuclear peak at \((1 0 1)\), a very weak magnetic peak was found at \((1 0 0)\) characterized by the propagation vector \(\mathbf{\tau} = (0 0 1)\) as observed before. Very strong intensity at the weakest nuclear peaks and the absence of incommensurate peaks indicate that the magnetic unit cell might be the same as the chemical unit cell with magnetic propagation vector \(\mathbf{\tau} = (0 0 0)\). Therefore, rocking scans for several representative nuclear peaks at \(T = 2\) and 25 K were performed to verify if there is any magnetic contribution superimposed on the nuclear peaks. These scans are shown in Figs. 5(a)–5(f). It is clear from the \(\omega\) scans of the \((0 0 L)\) reflections with \(L = 0\) in Figs. 5(a)–5(c) that they have identical intensities at 2 and 25 K, indicating the absence of magnetic signal at these positions. However, the weakest nuclear peaks \((1 1 0)\) and \((1 0 1)\), in Figs. 5(d) and 5(e) show very strong magnetic signals as the intensity of these reflections almost vanishes at 25 K. For the strong nuclear peak \((1 1 2)\), magnetic signal can be observed on top of the nuclear signal, as shown in Fig. 5(f). The absence of magnetic intensity for the \((0 0 L)\) reflections with \(L\) even as well as strong intensity at the \((1 1 0)\) position indicates that the moments are primarily along the \(c\) direction. Figures 5(g)–5(i) show \(\omega\) scans of the magnetic peaks associated with the minor phase. The FWHM of the \(\omega\) scans for the minor phase \(\sim 1.5^\circ\) is much larger than the main phase \(\sim 0.5^\circ\), indicating weak magnetic correlations or an incoherently grown minor phase.

Figure 6(a) shows temperature dependencies of the integrated intensities for the \((1 1 0)\) and \((1 0 1)\) reflections. No hysteresis was observed between the heating and cooling cycles, indicating the second-order nature of the phase transition. The integrated intensity \(I \sim m^2\), where \(m\) is the sublattice magnetization) can be fitted with a power law of the form \(I \sim (1 - C/T)^{\beta}\) to obtain a transition temperature of the \(Eu^{2+}\) magnetic order \(T_c = 19.0(1)\) K and an exponent \(\beta = 0.36(4)\). Since the \((1 0 1)\) reflection is sensitive to both in- and out-of-plane magnetic components, the identical nature of the temperature dependencies for both reflections indicates that the spin canting out of plane, if any, remains constant over the whole temperature range. Figure 6(b) shows temperature dependencies of the \((0 0 2.95)\) and \((1 0 0)\) magnetic reflections corresponding to the antiferromagnetic ordering of the \(Eu^{2+}\) moments associated with the minor phase. Using the same power-law fitting to the integrated intensity, antiferromagnetic ordering temperature, \(T_K = 17.0(2)\), and \(\beta = 0.27(3)\) could be obtained. The exponent for the major phase is close to that \((0.36)\) (Ref. [30]) of the three-dimensional (3D) classical Heisenberg model, typical for rare-earth elements in intermetallic compounds [31,32]. Surprisingly, the minor phase orders magnetically at a slightly lower temperature than the major phase, further hinting towards two independent magnetic phases. A decrease in ordering temperature, as has been observed for the underdoped region of the phase diagram, might indicate that the minor phase is located in the underdoped region in the phase diagram [20,22]. At low temperatures, the intensities of the reflections from the major and minor phases were fitted using FULLPROF [33] after necessary absorption correction using DATAP [34]. For the major phase, a ferromagnetic structure of the \(Eu^{2+}\) moments along the \(c\) direction was assumed (as concluded in the next section). The intensities of the minor phase (a total of eight magnetic reflections) were fitted with an A-type antiferromagnetic structure of the \(Eu^{2+}\) moments [13], with the moment size the same as that of the major phase. Comparing the scale factors for the major phase and minor phase, we estimate the volume fraction of the minor phase to be \((1.5 \pm 0.4)\).
C. Magnetic structure of the Eu$^{2+}$ moments

We now turn to the determination of the magnetic moment configuration for the Eu$^{2+}$ moments in the major phase. Here we note that only ferromagnetic structures with magnetic moments along the three crystallographic directions $a$, $b$, and $c$ are allowed by symmetry. No antiferromagnetic structure with $\tau = (0 \, 0 \, 0)$ is possible in this case for symmetry reasons. Since for magnetic neutron scattering, the scattered intensity is sensitive to the component of the magnetic moment perpendicular to $Q$, the absence of magnetic intensity for the nuclear (0 0 $L$) reflections [see Figs. 5(a)–5(c)] indicates that the moments are primarily along the $c$ direction. However, to put an upper limit on the canting angle as well as to determine the moment size, a magnetic structure refinement is needed. Conventional magnetic structure refinement using integrated intensity is difficult in this case (a) because the number of measured reflections is limited due to the use of thermal neutrons in a triple-axis spectrometer and (b) due to the errors associated with the resolution effects and absorption corrections in determining absolute integrated intensities. In particular, absorption correction is difficult with an irregularly shaped sample, as shown in the inset to Fig. 1. To circumvent these problems, we have refined the magnetic structure using the ratios of intensities between 2 and 25 K, i.e., using $R = I(2 \, K)/I(25 \, K) = 1 + I_M/I_N$, assuming the nuclear intensity $I_N$ does not vary between 2 and 25 K. By using the ratios of intensities, one can exclude the artifacts due to the resolution effects in a triple-axis spectrometer as well as absorption corrections. The intensity ratios measured for equivalent reflections and for repeated measurements of the same reflection were averaged together to give a mean value of the ratio and are shown in Fig. 7 together with the calculated ratios. The procedure for calculating intensity ratios is outlined below and has been implemented using MATHEMATICA [35].

The cross section for the magnetic neutron scattering can be written as [36]

$$\left(\frac{d\sigma}{d\Omega}\right)^M_{el} = (yr_0)^2 N_M \frac{(2\pi)^3}{\nu_{min}} \sum_{\bar{r}_m} |F_m(\bar{r}_m)|^2 \times \left\{ 1 - (\hat{\theta} \cdot \hat{n})^2 \right\} \delta(\hat{k} - \bar{r}_m),$$

(1)
where

\[ F_m(\vec{r}_m) = \frac{1}{2} g \langle \vec{S} \rangle f(\vec{r}_m) \sum_d \sigma_d \exp(i \vec{r}_m \cdot \vec{d}) \exp(-w_d). \]

Here, \( \gamma r_0 = 5.36 \times 10^{-15} \text{ m}, N_M = \text{number of magnetic unit cells in the crystal}, v_m = \text{volume of the magnetic unit cell}, \vec{r}_m = \text{vector in magnetic reciprocal lattice}, \text{and} w_d = \text{the Debye-Waller factor (DWF)}. \hat{n} = \text{direction of spin} \vec{S} \text{ where} “av” \text{means average over domains} \) [37]. \( g \) \text{is the Landé g factor and} f(\vec{r}_m) \text{is the magnetic form factor at the scattering vector} \vec{r}_m, \sigma_d = 1 \text{in this case and} \vec{d} \text{denotes magnetic atoms in the magnetic unit cell.}

Similarly, the coherent elastic nuclear-scattering cross section can be written as

\[ \left( \frac{d\sigma}{d\Omega} \right)_{\text{elastic}} = N_N \frac{(2\pi)^3}{v_0} \sum_{\vec{r}_m} |F_N(\vec{k})|^2 \delta(\vec{k} - \vec{r}_m), \]

\[ F_N(\vec{k}) = \sum_d \bar{b}_d \exp(i \vec{k} \cdot \vec{d}) \exp(-w_d). \]  

FIG. 6. (Color online) Temperature dependence of the integrated intensity for the (1 1 0) reflection measured during heating and cooling and for the (1 0 1) reflection measured during heating. (b) For comparison, we also show the temperature dependencies of the (0 0 2.95) and (1 0 0) reflections corresponding to the minor phase. The solid lines are fit to the data as described in the text.

where symbols have the usual meaning similar to magnetic scattering and \( \bar{b}_d \) \text{is the nuclear-scattering length for the} d \text{th ion}. The integrated intensity of a reflection at a scattering angle \( 2\theta \) can be written as

\[ I = \frac{V}{v_0^2} \phi \lambda^3 \times A(\theta) \times B(\mu) \times y_s \times \frac{d\sigma}{d\Omega}, \]

where \( V \) \text{is the volume of the crystal}, \( \phi \) \text{is the incident neutron flux}, \( A(\theta) \) \text{contains angular-dependent factors such as Lorentz factor and resolution factor}, and \( B(\mu) \) \text{is the absorption correction factor. The secondary extinction correction factor} y_s \text{depends on the mosaic width, scattering angle, and average scattering cross section for a particular reflection. It can be seen from Eqs. (1)–(3) that in the calculated ratio, all factors except (i) absolute value of the moment, (ii) moment direction, (iii) DWF, and (iv) extinction correction cancel out. However, in a conventional single-crystal neutron-diffraction experiment on similar compounds, it was found that the extinction corrections are small and so we will neglect them in the subsequent analysis. Fitting the nuclear intensities at} \ T = 25 \text{ K with and without an extinction parameter (not shown)} \]

FIG. 7. (Color online) Comparison between the observed ratio \( (R_{\text{obs}}) \), fitted ratio \( (R_{\text{fit}}) \), and calculated ratio \( (R_{\text{cal}}) \) for the measured reflections. Details have been outlined in the text.

TABLE I. Parameters used for least-square refinement of the ratios [13,29]. Occupancies corresponding to the As and P sites were fixed according to the chemical composition.

| Atom | Position in I4/mmm | B (Å²) | n |
|------|--------------------|--------|---|
| Eu   | 2a                 | 0      | 0 | 0.8 | 1.00 |
| Fe   | 4d                 | 0      | 0 | 0.3 | 1.00 |
| As   | 4e                 | 0      | 0 | 0.3615 | 0.3 | 0.81 |
| P    | 4e                 | 0      | 0 | 0.3615 | 0.3 | 0.19 |

\[ a = 3.91(2) \text{ Å}, c = 11.77(4) \text{ Å} \]
TABLE II. The observed, fitted, and calculated ratios for the reflections with magnetic contribution of EuFe$_2$(As$_{0.81}$P$_{0.19}$)$_2$. Various cases have been considered as described in the footnotes and in the main text.

| h  | k  | l  | $\sin \theta/\lambda$ | $R_{obs}$ | $R_{calc}$ | $\chi^2/a$ | $\chi^2/b$ | $\chi^2/c$ | $\chi^2/d$ | $\chi^2/e$ |
|----|----|----|------------------------|-----------|-----------|-------------|-------------|-------------|-------------|-------------|
| 0  | 0  | 2  | 0.0851                 | 98.8 ± 1.4| 100.1     | 100.0       | 100.0       | 104.2       | 111.7       | 104.4       |
| 0  | 0  | 4  | 0.1702                 | 99.9 ± 1.4| 100.1     | 100.0       | 102.9       | 107.9       | 103.0       | 111.7       |
| 0  | 0  | 6  | 0.2553                 | 100.6 ± 2.4| 100.3     | 100.0       | 110.2       | 128.5       | 110.7       | 141.7       |
| 1  | 1  | 2  | 0.2000                 | 118.8 ± 3.5| 124.0     | 124.0       | 122.9       | 116.0       | 124.1       | 123.5       |
| 1  | 1  | 4  | 0.2485                 | 114.4 ± 4.4| 111.5     | 111.5       | 111.2       | 108.3       | 117.1       | 112.2       |
| 1  | 1  | 6  | 0.3129                 | 96.7 ± 3.0 | 102.5     | 102.5       | 102.5       | 102.0       | 102.6       | 102.9       |
| 2  | 1  | 3  | 0.3134                 | 127.2 ± 14.0| 120.1     | 120.0       | 119.1       | 113.3       | 120.1       | 119.6       |
| 2  | 2  | 0  | 0.3620                 | 104.5 ± 7.6| 103.4     | 103.4       | 103.2       | 102.2       | 103.4       | 103.3       |
| 1  | 0  | 3  | 0.1808                 | 129.8 ± 1.8| 128.9     | 128.9       | 128.3       | 121.1       | 129.7       | 130.9       |
| 1  | 0  | 5  | 0.2483                 | 122.5 ± 2.0| 124.9     | 124.9       | 125.7       | 121.8       | 126.9       | 131.9       |
| 2  | 0  | 0  | 0.2559                 | 104.2 ± 1.8| 107.8     | 107.8       | 107.4       | 105.1       | 107.8       | 107.5       |
| 2  | 0  | 2  | 0.2698                 | 150.9 ± 2.4| 147.9     | 148.0       | 145.6       | 131.6       | 147.9       | 146.3       |
| 2  | 0  | 4  | 0.3074                 | 128.4 ± 3.0| 128.5     | 128.5       | 127.4       | 119.6       | 128.8       | 128.7       |

Parameters: $m_{Eu} = 6.6(2) \mu_B$, $m_{Fe} = 6.6(2) \mu_B$, $m_{As} = 6.5(5) \mu_B$, $m_{P} = 6.6 \mu_B$, $m_{Eu} = 6.6 \mu_B$.

Quality factors: $\chi^2 = \frac{\sum w_p (I_{obs} - I_{calc})^2}{\sum w_p}$, $w_p = 1/\sigma_p^2$ is the weight where $\sigma_p^2$ is the variance of $I_{obs}$.

- $R_{wp} = 3.3\%$, $R_{wp} = 3.2\%$, $R_{wp} = 6.7\%$, $R_{wp} = 15.8\%$.
- $\theta = 2(6)^\circ$, $\theta = 0^\circ$, $\theta = 10^\circ$, $\theta = 20^\circ$.
- $X_{\chi^2} = 1.34$, $X_{\chi^2} = 1.22$, $X_{\chi^2} = 3.8$, $X_{\chi^2} = 25.0$.

*Fitted with $m_{Eu}$ and canting angle $\theta$.

*Fitted with $m_{Eu}$ and canting angle was fixed to 0, 10, 20$^\circ$.

*Calculated with $m_{Eu} = 6.6 \mu_B$ and $\theta = 10^\circ$.

*Calculated with $m_{Eu} = 6.6 \mu_B$ and $\theta = 20^\circ$.

Clearly demonstrates that the extinction can be neglected. In fact, adding an extinction parameter worsens the quality of fit. For the accurate determination of the DWF, a conventional neutron-diffraction experiment up to high $Q$ is needed. We have used the DWF’s for the parent compound [13] and used the same DWF for P as for As. Furthermore, we have compared our results without applying any DWF and the results are the same within errors. For the estimation of the nuclear intensity, the $z$ position of As, $z$(As), is required. Since the $z$(As) varies from 0.363 for the parent compound to 0.360 for the end member, we have used 0.3615 for the calculation of the nuclear intensity. All of the structural parameters used in the refinement are listed in Table I. We have excluded in the refinement the very weak nuclear reflections with very strong magnetic contributions such as (1 1 0), (1 0 1), and (2 1 1) since the intensity of these reflections slowly decreases above $T_C$. The resulting fitted ratios are shown along with the observed ratios in Fig. 7. We obtained magnetic moment size of Eu$^{2+}$, $m_{Eu} = 6.6(2) \mu_B$ with possible canting angle $\theta = 2(6)^\circ$ with the aid of MATHEMATICA [35]. The magnetic moment size is close to the theoretically predicted value of $7 \mu_B$ for a $J = 7/2$ Eu$^{2+}$ ion.

Here we note that the canting angle of 2$^\circ$ from the fitting of the ratios is much smaller than the reported values of Ryan et al. [29] as well as Nowik et al. [25] of approximately 20$^\circ$. Therefore, we have considered five different scenarios, namely, we fitted the ratios with canting angle fixed to 0, 10, and 20$^\circ$ (Table II, footnotes b–d), respectively, and simulated the ratios with moment size fixed to 6.6 $\mu_B$ and two different canting angles, 10 and 20$^\circ$ (Table II, footnotes e and f), respectively. The simulated results are shown in Fig. 7 and both the fitted and simulated results are summarized in Table II. It can be clearly seen that the (0 0 L) reflections deviate strongly from the observed ratio if any canting angle is added. The deviation is strongest for the (0 0 6) reflection. Therefore, the measurement of accurate integrated intensities for weak reflections such as (0 0 6) using a triple-axis spectrometer provides the strongest constraint on the canting angle. Fitting with any canting angle is poor, as can be seen from the obtained ratios as well as agreement factors in Table II. Fitting without any canting angle ($\theta = 0^\circ$) produces the best $X_{\chi^2}$ for the calculated ratios. Therefore, we conclude that the canting angle is zero in the present case, i.e., moments are aligned along the $c$ direction.

IV. CONCLUSION

In conclusion, the magnetic structure of the Eu$^{2+}$ moments in the superconducting EuFe$_2$(As$_{1-x}$P$_x$)$_2$ sample with $x = 0.19$ has been determined using neutron scattering. We conclude that the Eu$^{2+}$ moments order along the $c$ direction below $T_C = 19.0(1)$ K with an ordered magnetic moment of 6.6(2) $\mu_B$ in the superconducting state. An impurity phase similar to the underdoped phase exists within the bulk sample which orders antiferromagnetically below $T_N = 17.0(2)$ K. Further measurements are necessary to elucidate the exact nature of the minor phase. We found no indication of iron magnetic order, nor an incommensurate magnetic order of the Eu moments associated with the major phase.
The proposed canted antiferromagnetic order could not be detected in the superconducting sample. It will be interesting to investigate Eu magnetic order for a higher doping level in the EuFe$_2$(As$_{1-x}$P$_x$)$_2$ system using single-crystal neutron diffraction.

**ACKNOWLEDGMENTS**

S.N. acknowledges S. Zapf and M. Dressel for fruitful discussion. Work at Georg-August-Universität Göttingen was supported by the German Science Foundation through Grant No. SPP 1458.