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Citation
Lacki, Brian C., Todd A. Thompson, Eliot Quataert, Abraham Loeb, and Eli Waxman. 2011. "ON THE GeV AND TeV DETECTIONS OF THE STARBURST GALAXIES M82 AND NGC 253." The Astrophysical Journal 734 (2): 107. https://doi.org/10.1088/0004-637x/734/2/107.

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ON THE GeV AND TeV DETECTIONS OF THE STARBURST GALAXIES M82 AND NGC 253

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Received 2010 March 16; accepted 2011 April 7; published 2011 June 3

ABSTRACT

The GeV and TeV emission from M82 and NGC 253 observed by Fermi, HESS, and VERITAS constrain the physics of cosmic rays (CRs) in these dense starbursts. We argue that the γ-rays are predominantly hadronic in origin, as expected by previous studies. The measured fluxes imply that pionic losses are efficient for CR protons in both galaxies: we show that a fraction $F_{\text{cal}} \approx 0.2-0.4$ of the energy injected in high-energy primary CR protons is lost to inelastic proton–proton collisions (pion production) before escape, producing γ-rays, neutrinos, and secondary electrons and positrons. We discuss the factor of ~2 uncertainties in this estimate, including supernova rate and leptonic contributions to the GeV–TeV emission. We argue that γ-ray data on ULIRGs like Arp 220 can test whether M82 and NGC 253 are truly calorimetric, and we present upper limits on Arp 220 from the Fermi data. We show that the observed ratio of the GeV to GHz fluxes of the starbursts suggests that non-synchrotron cooling processes are important for cooling the CR electron/positron population. We briefly reconsider previous predictions in light of the γ-ray detections, including the starburst contribution to the γ-ray background and CR energy densities. Finally, as a guide for future studies, we list the brightest star-forming galaxies on the sky and present updated predictions for their γ-ray and neutrino fluxes.

Key words: cosmic rays – galaxies: individual (M82, NGC 253) – galaxies: starburst – gamma rays: galaxies – radio continuum: galaxies

1. INTRODUCTION

M82 and NGC 253 are nearby ($D \approx 2.5–4.0$ Mpc), prototypical starburst galaxies, each having an intense star-forming region of about 200 pc radius in the center of a more quiescent disk galaxy. The starbursts are expected to have high supernova (SN) rates of about 0.03–0.3 yr$^{-1}$. SN remnants are believed to accelerate primary cosmic ray (CR) protons and electrons. The high SN rates in starbursts imply high CR emissivities. The presence of CR electrons and positrons in these starbursts is inferred from the nonthermal synchrotron radio emission they produce (e.g., Klein et al. 1988; Völk et al. 1989; Condon 1992). However, most of the CR energy is believed to be in the form of CR protons.

When high-energy CR protons collide with interstellar medium (ISM) nucleons, they create pions, which decay into γ-rays, neutrinos, and secondary electrons and positrons. With their dense ISMs ($\langle n \rangle \approx 100–500$ cm$^{-3}$) and possible high CR energy densities (as evinced by the bright radio emission; Völk et al. 1989; Akyuz et al. 1991; Persic & Rephaeli 2010), M82 and NGC 253 are predicted to be bright γ-ray sources (e.g., Akyuz et al. 1991; Sreekumar et al. 1994; Völk et al. 1996; Paglione et al. 1996; Romero & Torres 2003; Domingo-Santamaria & Torres 2005; Thompson et al. 2007, hereafter TQW; Persic et al. 2008; de Cea del Pozo et al. 2009a; Rephaeli et al. 2010; Lacki et al. 2010, hereafter LTQ). As prototypical starbursts, if M82 and NGC 253 are seen in γ-rays, starbursts in general may be sources of γ-rays (Pohl 1994; Torres et al. 2004), with important implications for the diffuse γ-ray and neutrino backgrounds (e.g., Pavlidou & Fields 2002; Loeb & Waxman 2006, hereafter LW06; TQW). However, the γ-ray luminosity of starbursts depends not only on the injection rate of CRs, but also on the efficiency of converting CR proton energy into pion γ-rays, neutrinos, and secondary electrons and positrons. In turn, this efficiency depends on the ratio of the timescale for pion production to the escape timescale. The hypothesis that CR protons in starbursts lose all of their energy to pionic collisions before escaping is called “proton calorimetry” (cf. Pohl 1994). If proton calorimetry is strongly violated, then M82 and NGC 253 and, by extension, other starbursts could in fact be weak γ-ray sources.

Although γ-ray emission from M82 and NGC 253 has been sought for several years with no success (at GeV, Cilliss et al. 2005; and at TeV, Aharonian et al. 2005, Itoh et al. 2007), the launch of Fermi and the advent of powerful very high energy (VHE) γ-ray telescopes has led to recent detections of both starbursts at GeV energies (with Fermi; Abdo et al. 2010a) and in VHE γ-rays (M82 with VERITAS, Acciari et al. 2009; NGC 253 with HESS, Acero et al. 2009). These GeV and TeV detections constrain the CR population in these dense star-forming environments.

In this paper, we discuss the implications of the γ-ray detections of M82 and NGC 253. The ratio of the γ-ray luminosities to the bolometric luminosities informs the question of whether or not these systems are proton calorimeters (TQW). The emission also has implications for the energy density of CRs in starbursts (e.g., Akyuz et al. 1991). Finally, combined with the radio emission, the energy losses of CR electrons and positrons are constrained (cf. Paglione et al. 1996; Domingo-Santamaria & Torres 2005; Persic et al. 2008; de Cea del Pozo et al. 2009a; Rephaeli et al. 2010). Pionic γ-rays must be accompanied by

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secondary positrons and electrons; the ratio of the power in these expected electrons and positrons to the observed radio emission informs us of the energy losses of the CR electrons and positrons. In particular, we derive in Section 5 the expected synchrotron luminosity from the pionic luminosity if synchrotron cooling is the dominant loss process.

In Section 2, we describe the detections of M82 and NGC 253 at GeV and TeV energies. We then interpret the detections as γ-rays from diffuse CR protons in Section 3. Our interpretation includes comparison of the γ-ray luminosities of M82 and NGC 253 with their CR luminosities and their infrared (IR) luminosities (Section 3.2), and a discussion of the uncertainties in these estimates (Section 3.3). We find that a fraction 0.4 and 0.2 of luminosity in ≥GeV CR protons is lost to pion production in M82 and NGC 253, respectively. We discuss the implications for our estimates mean for proton calorimetry in M82 and NGC 253 at GeV energies (Section 3.4). Other possible sources for the observed γ-rays are considered in Section 4. The implications of the detections of M82 and NGC 253 for the detection of other star-forming galaxies, the starburst contribution to the diffuse extragalactic γ-ray and neutrino backgrounds, the dynamical importance of CRs in starbursts, and for the physics of the FIR–radio correlation are described in Section 6. We summarize our results in Section 7.

2. γ-RAY DETECTIONS

2.1. Fermi and TeV Detections

Abdo et al. (2010a) reported the detections of M82 (6.8σ) and NGC 253 (4.8σ) with the Fermi Large Area Telescope (LAT) instrument. At energies above a few hundred MeV, the γ-ray spectrum of starburst galaxies is expected to be described by a power-law spectrum with differential photon fluxes \( N(E) = N_0(E/E_0)^{-\Gamma} \), where \( \Gamma \) (~2) is the photon spectral index (e.g., Paglione et al. 1996). Using the GeV data point as a normalization, we adopt GeV differential fluxes of

\[
N_{\text{M82}} \approx 1.9_{-0.4}^{+0.5} \times 10^{-9} \left( \frac{E}{\text{GeV}} \right)^{-\Gamma} \text{ph cm}^{-2} \text{s}^{-1} \text{GeV}^{-1}
\]

\[
N_{\text{NGC 253}} \approx 0.9_{-0.3}^{+0.4} \times 10^{-9} \left( \frac{E}{\text{GeV}} \right)^{-\Gamma} \text{ph cm}^{-2} \text{s}^{-1} \text{GeV}^{-1}.
\]

The Abdo et al. (2010a) maximum likelihood analysis of the sources find \( \Gamma \) of 2.2 ± 0.2 ± 0.05 for M82 and 1.95 ± 0.4 ± 0.05 for NGC 253; however, the Fermi photon statistics are insufficient for accurate measurements of \( \Gamma \). Using the best-fit power laws in Abdo et al. (2010a) gives GeV normalizations that are 60%–70% of those in Equations (1) and (2), although these fits are influenced by the nondetections at lower and higher energies. Fermi has not detected either starburst above ~20 GeV, and NGC 253 is undetected below ~500 MeV. The reported spectra are shown in Figure 1.

Assuming a power-law spectrum from GeV to VHE energies, we can combine the Fermi detections with the HESS and VERITAS measurements to derive the spectral slope over this energy range. The integrated fluxes from M82 reported by VERITAS (at 1.3–3.8 TeV) correspond to GeV–VHE spectral slopes \( \Gamma \) of 2.19–2.25 (Acciari et al. 2009), in excellent agreement with the measured spectral slope from Fermi. The HESS detection of NGC 253 at 220 GeV implies \( \Gamma = 2.3 \) (Acero et al. 2009), steeper than the best-fit photon index from the Fermi detections, but within the quoted errors. We adopt \( \Gamma = 2.2 \) for M82 and \( \Gamma = 2.3 \) for NGC 253 throughout the rest of this paper.

Our values of \( \Gamma \) are only appropriate if the spectrum is truly a single power law between GeV and TeV energies. A spectral bump at GeV energies will cause an underlying pionic power-law spectrum to appear steeper than it really is; conversely, a
spectral bump at TeV energies will cause it to appear flatter. The possibility of a “GeV excess” is notable particularly because such an excess is seen in the Milky Way (Prodanović et al. 2007; Abdo et al. 2008; see Section 4.3).

Figure 1 shows that the γ-ray spectra of both M82 and NGC 253 are in reasonable agreement with most of the previous detailed model predictions (Domingo-Santamaría & Torres 2005; Persic et al. 2008; de Cea del Pozo et al. 2009a; Rephaeli et al. 2010). However, these models slightly overpredict both the GeV flux and the ~400 MeV flux of NGC 253 by a factor of ~2–3. The Paglione et al. (1996) model greatly overestimates the ≲GeV flux by a factor of ~5 (although it used a higher CR acceleration efficiency), and predicts a much softer spectrum (Γ ≈ 2.7) than observed. Overall, the general agreement between the theory and observations of γ-rays from M82 and NGC 253 is encouraging (see also de Cea del Pozo et al. 2009b), and suggests that models of other starbursts, particularly Arp 220 (Torres 2004; LTQ), also predict their γ-ray fluxes with fidelity (Section 6.1).

2.2. M82 and NGC 253 Gamma-ray Luminosities

For a dN/dE = N_0(E/E_0)^{-Γ} γ-ray spectrum from E_{min} to E_{max}, the total luminosity at energies higher than E_{min} is

\[ L_{γ}(≥E_{min}) = 2.4 \times 10^{39} \text{ erg s}^{-1} \ N_{-9} D_{3.5}^2 β_γ, \]

where \( N_{-9} = N_0/(10^{-9} \text{ ph cm}^{-2} \text{ s}^{-1} \text{ GeV}^{-1}) \), \( D_{3.5} = D/3.5 \text{ Mpc} \), and

\[ \beta_γ = \begin{cases} (Γ - 2)^{-1} \left[ 1 - \left( \frac{E_{min}}{E_{max}} \right)^{2-Γ} \right] & (Γ ≠ 2) \\ \ln \left( \frac{E_{max}}{E_{min}} \right) & (Γ = 2). \end{cases} \]

Typically, \( β_γ ≈ 2–5 \).

The GeV flux reported by Fermi for M82 is \( N_{-9} = 1.9^{+0.5}_{-0.4} \), and the VERITAS detections imply a \( Γ ≈ 2.2 \) spectrum extending to at least \( E_{max} = 3.8 \text{ TeV} \). This corresponds to a ≥GeV luminosity of

\[ L_{M82}(≥GeV) = 1.9^{+0.5}_{-0.4} \times 10^{40} \text{ D}_{3.5}^2 \text{ erg s}^{-1}. \]

If we interpret the HESS detection of NGC 253 as part of a single \( Γ ≈ 2.3 \) power law extending at least to \( E_{max} = 220 \text{ GeV} \), and use the \( N_{-9} = 0.9^{+0.4}_{-0.3} \) value from Abdo et al. (2009a), we find that the GeV luminosity of NGC 253 is

\[ L_{NGC 253}(≥GeV) = 5.6^{+2.5}_{-1.9} \times 10^{39} \text{ D}_{3.5}^2 \text{ erg s}^{-1}. \]

As \( E_{max} → ∞ \), the luminosity increases by only ~25%. In light of the harder Fermi best-fit spectrum to the GeV data (\( Γ = 1.95 ± 0.4 ± 0.05 \)), the VHE emission might be a different spectral component (perhaps pulsar wind nebulae (PWNe); see Section 4.2 and Mannheim et al. 2010) if the pionic emission falls off between 20 and 200 GeV. However, a harder spectrum with lower \( E_{max} \) still implies a similar γ-ray luminosity (~(7–11) × 10^{39} \text{ D}_{3.5}^2 \text{ erg s}^{-1}) with those assumptions, and the Fermi data are not accurate enough to conclude there is a discrepancy.

3. INTERPRETATION AS PIONIC EMISSION

3.1. Motivation for Proton Calorimetry

The hypothesis that starbursts are proton calorimeters is motivated by the short pionic energy loss time in their dense ISMs,

\[ τ_p ≈ 2 × 10^{5} \text{ yr} \left( \frac{n_{eff}}{250 \text{ cm}^{-3}} \right)^{-1}, \]

where \( n_{eff} \) is the average density of the ISM encountered by CR protons before escape (Mannheim & Schlickeiser 1994), and the mean gas density in the starbursts of M82 and NGC 253 is a few hundred cm^{-3}.

If \( τ_p \) is less than the escape timescale, then the system is a proton calorimeter. CRs may escape by advection in galactic winds or by diffusion. The wind advection time is

\[ τ_{wind} ≈ h/v ≈ 2 × 10^{5} \text{ yr} h_{100} v_{500}^{-1}, \]

for a scale height of \( h = 100 h_{100} \text{ pc} \) and wind speed of \( v = v_{500} \text{ km s}^{-1} \). We expect the diffusive escape time to go as \( t_{diff}(E) = t_0(E/E_0)^{-2/3} \), where \( t_0 = 26 \text{ Myr} \) at \( E_0 = 3 \text{ GeV} \) in our Galaxy from radioactive isotopes in CRs (CR clocks; Connell 1998; Webber et al. 2003). Little is known about the diffusion escape time in starbursts (for example, Domingo-Santamaría & Torres 2005 and de Cea del Pozo et al. 2009a assume \( t_{diff} ≈ 1–10 \text{ Myr} \)). If we assume that CRs stream out of the starbursts at the average Alfvén speed \( v_A = B/\sqrt{4πρ} \) (Kulsrud & Pearce 1969), then

\[ t_{diff} ≈ 3.5 \text{ Myr} h_{100} B_{200}^{-1} v_{500}^{1/2}, \]

where \( B_{200} = B/(200 \mu \text{ G}) \) and \( n_{250} = n/(250 \text{ cm}^{-3}) \).

From Equations (7) to (9), pionic losses dominate advection losses if \( n_{eff} ≥ 250 \text{ cm}^{-3} h_{100} v_{500}^{-1} \), and diffusive losses at a few GeV if \( n_{eff} ≥ 40 \text{ cm}^{-3} B_{200}^{-3/2} h_{100}^{-1} \), again assuming CRs stream out of the starbursts at the Alfvén speed. We see that the advective and pionic loss times are roughly equal in M82 and NGC 253, implying that inelastic proton–proton collisions are an important loss process for GeV protons, and suggesting proton calorimetry (LW06; TQW).

There are two ways to avoid this conclusion: more efficient escape (shorter \( t_{adv} \) or \( t_{diff} \)), or less efficient pion losses (longer \( τ_p \), smaller \( n_{eff} \)). Both are possible. In particular, there may be a fast wind component with \( v ≈ 1000–2000 \text{ km s}^{-1} \) from M82 (Strickland & Heckman 2009), although Heesen et al. (2009) find wind speeds \( v ≈ 300 \text{ km s}^{-1} \) in the halo of NGC 253. In addition, the pionic losses are less efficient if the CRs mainly travel through low-density gas. The ISM in starbursts is clumpy, with most of the volume contained in a low-density phase (e.g., Lord et al. 1996; Mao et al. 2000; Rodriguez-Rico et al. 2004; Westmoquette et al. 2009). Indeed, there is γ-ray and radio evidence that CRs do not penetrate deep into molecular clouds in the Galactic center, so that \( n_{eff} ≪ \langle n \rangle \) and proton calorimetry fails (Crockser et al. 2011a, 2011b).

If either advective losses or pionic losses dominate, the CR proton and hadronic γ-ray spectra should both be relatively hard with \( Γ ≈ 2.0–2.4 \) for standard injection spectra. This is because the equilibrium one-zone CR proton spectrum is roughly \( N(E) ∝ Q(E) τ(E) \), where \( Q(E) ∝ E^{-p} \) is the proton injection spectrum with \( 2.0 ≤ p ≤ 2.4 \) expected, and \( τ(E) \) is the CR proton lifetime including escape and (catastrophic) pion losses. Both the advective and pionic lifetimes are roughly energy-dependent, so they preserve the hard injection spectrum. By

\[ L_{M82}(≥GeV) = 1.9^{+0.5}_{-0.4} \times 10^{40} \text{ D}_{3.5}^2 \text{ erg s}^{-1}. \]

As \( E_{max} → ∞ \), the luminosity increases by only ~25%. In light of the harder Fermi best-fit spectrum to the GeV data (\( Γ = 1.95 ± 0.4 ± 0.05 \)), the VHE emission might be a different spectral component (perhaps pulsar wind nebulae (PWNe); see Section 4.2 and Mannheim et al. 2010) if the pionic emission falls off between 20 and 200 GeV. However, a harder spectrum with lower \( E_{max} \) still implies a similar γ-ray luminosity (~(7–11) × 10^{39} \text{ D}_{3.5}^2 \text{ erg s}^{-1}) with those assumptions, and the Fermi data are not accurate enough to conclude there is a discrepancy.
observed which we estimate $F_{\text{cal}}$ is available at http://galprop.stanford.edu. The harder $\gamma$-ray spectra of M82 and NGC 253 support either proton calorimetry or strong advective losses.

3.2. Measuring the Calorimetry Fraction

We define $L_\pi$ as the power of the starburst in all pion end products, including hadronic $\gamma$-rays, neutrons, and secondary electrons and positrons. The ratio of $L_\pi$ to the injected CR luminosity ($L_{\text{CR}}$) for CR protons with kinetic energy per particle ($K$) above the pion-production threshold ($K_{\text{th}}$) is then the "calorimetry fraction," which measures to which degree starbursts are calorimeters:

$$F_{\text{cal}} \equiv \frac{L_\pi}{L_{\text{CR}}(K > K_{\text{th}})} \approx \frac{t_{\text{life}}}{t_\pi}.$$  

(10)

The lifetime $t_{\text{life}}$ of CR protons with $K > K_{\text{th}}$ includes all losses—pionic, ionization, diffusive, and advective. If proton calorimetry holds, then $t_{\text{life}} \approx t_\pi$, $L_\pi \approx L_{\text{CR}}(K > K_{\text{th}})$, and $F_{\text{cal}} \rightarrow 1$. In what follows, we restrict the energy range over which we estimate $F_{\text{cal}}$ to be $\geq 1$ GeV. In particular, we use observed $\gamma$-rays with energies $\geq 1$ GeV to estimate $L_\pi$ for CRs with $K \geq 1$ GeV. While a significant fraction of both the pionic $\gamma$-rays and the CRs have energies below 1 GeV, leptonic emission is expected to become increasingly important at lower energies, contaminating the estimate of the proton calorimetry fraction.

The total injected CR power $L_{\text{CR}}$ likely scales with the star formation rate (SFR; cf. Abdo et al. 2010), and concomitantly, the SN rate, $\Gamma_{\text{SN}}$. Assuming that with each SN, a fraction $\eta^1$ of its kinetic energy goes to primary CR protons with $K \geq 1$ GeV,

$$L_{\text{CR}}(\geq \text{GeV}) = 3.2 \times 10^{41} \text{ erg s}^{-1} E_{51} \eta^1_0 \Gamma_{\text{SN},0.1},$$  

(11)

where $\eta^1_0 = \eta^1/0.1$, $E_{51}$ is the energy of the SN in $10^{51}$ erg, and $\Gamma_{\text{SN},0.1} = \Gamma_{\text{SN}}/0.1 \text{ yr}^{-1}$.

Even in the proton calorimetric limit ($F_{\text{cal}} \rightarrow 1$), the GeV $\gamma$-ray luminosity will be significantly smaller than $L_{\text{CR}}$. First, only $\sim 1/3$ of $L_\pi$ ends up as $\gamma$-rays; $L_\pi \approx 3L_\pi$. Second, a fraction $\beta_\pi$ of the pionic $\gamma$-rays from CR protons with $K \geq $ GeV will have energies $> \text{GeV}$. We calculate $\beta_\pi$ using GALPROP pionic cross sections (Moskalenko & Strong 1998; Strong & Moskalenko 1998; Strong et al. 2000) based on the work of Dermer (1986) (see also Stecker 1970; Badhwar et al. 1977; Stephens & Badhwar 1981) and a $K^{-\rho}$ spectrum from 1 GeV to 1 PeV, and find that it ranges from 0.9 ($\rho = 2.0$) to 0.5 ($\rho = 2.5$). Using these factors (see Equation (3))

$$F_{\text{cal}} \approx 0.023 D_{3.5}^2 \eta^1_0 \beta_\pi^{-1} E_{51}^{-1} \eta^1_0 \Gamma_{\text{SN},0.1}.$$  

(12)

We expect that $\Gamma_{\text{SN}}$ is proportional to the luminosity from young massive stars and the SFR. Because most of the stellar luminosity is converted into IR light by dust in starbursts, if proton calorimetry holds, then the $\gamma$-ray flux of M82 and NGC 253 should simply be a fraction of the total FIR flux. Furthermore, if $\eta^1$ is constant for all starbursts, then this ratio of observed fluxes will be constant in the calorimeter limit, so that starbursts should lie on a linear "$\text{FIR}-\gamma$-ray correlation" in analogy with the FIR–radio correlation (TQW). Observations of normal and starburst galaxies do suggest some kind of correlation between SFR and $L_\pi$, but this correlation increases faster than linearly ($L_\pi(\gtrsim 100 \text{ MeV}) \propto \text{SFR}^{1.4\pm 0.3}$, Abdo et al. 2010), as expected if escape is more efficient in low-luminosity galaxies (cf. Strong et al. 2010).

Following TQW, we assume that SFR is related to the total FIR luminosity ($L_{\text{TIR}}$) by $L_{\text{TIR}} = \epsilon \text{SFR}^2$, where $\epsilon$ is an initial mass function (IMF)-dependent constant (see, e.g., Kennicutt 1998). In the calorimeter limit,$$

\frac{\xi_{\text{cal}}}{\xi_{\text{TIR}}} \equiv \frac{1}{\beta_\pi} \frac{L_\pi(\geq \text{GeV})}{L_{\text{TIR}}} \approx 3.1 \times 10^{-4} E_{51} \eta^1_0 \Gamma_{\text{SN},17},$$  

(13)

where $\Gamma_{\text{SN}} = (\Gamma_{\text{SN}}/\epsilon)/17 M_{\odot}^{-1}$ depends very modestly on the star formation history of the galaxy considered; it varies from $\sim 15$ to $\sim 23$ for continuous star formation over timescales of $3 \times 10^7$–$10^9$ yr (Leitherer et al. 1999; TQW).

We scale the TIR luminosities from Sanders et al. (2003) (see Tables 1 and 2) to the same distances as the $\gamma$-ray luminosities in Equations (5) and (6). For M82 ($\beta_\pi = 0.7$), we find that

$$F_{\text{cal}}^{\text{M82}} = \xi_{\text{cal}}^{\text{M82}} / \xi_{\text{cal}}^{\text{TIR}} \approx 0.4 (E_{51} \eta^1_0 \Gamma_{17})^{-1} \sim 10^{-2} \text{yr}^{-1}.$$  

(14)

For NGC 253, we find that $F_{\text{cal}}$ is

$$F_{\text{cal}}^{\text{NGC 253}} = \xi_{\text{cal}}^{\text{NGC 253}} / \xi_{\text{cal}}^{\text{TIR}} \approx 0.2 (E_{51} \eta^1_0 \Gamma_{17})^{-1} \sim 10^{-2} \text{yr}^{-1}$$  

(15)

for $\Gamma = 2.3$ (to 220 GeV) and $\beta_\pi \approx 0.6$. The flux uncertainties in the Fermi and HESS detections of NGC 253 indicate that the uncertainty in $F_{\text{cal}}^{\text{NGC 253}}$ can be significantly reduced by more Fermi data. Note that we have used the entire TIR flux of these galaxies, while the starburst cores (and not the outlying disks) probably dominate the $\gamma$-ray emission (see the treatments of NGC 253 by Domingo-Santamaría & Torres 2005; Rephaeli et al. 2010).

Alternatively, one may estimate $F_{\text{cal}}$ with a distance-independent SN rate (e.g., from radio source counts). In this case, $F_{\text{cal}}$ (Equation (10)) retains its strong distance dependence. For M82 ($D = 3.6 \text{ Mpc}$, $N_{\odot} = 2$, $\Gamma = p = 2.2$, $\beta_\pi = 0.7$, $\beta_\gamma = 3.96$),

$$F_{\text{cal}}^{\text{M82}} \approx 0.3 (E_{51} \eta^1_0)^{-1} D_{3.5}^2 \Gamma_{\text{SN},0.1}^{-1},$$  

(16)

where we have scaled to a value of $\Gamma_{\text{SN}}$ typically quoted in the literature. Similarly,

$$F_{\text{cal}}^{\text{NGC 253}} \approx 0.1 (E_{51} \eta^1_0)^{-1} D_{3.5}^2 \Gamma_{\text{SN},0.1}^{-1},$$  

(17)

for our adopted NGC 253 spectrum (see Equation (15)).

The higher numbers for $F_{\text{cal}}$ in Equations (14) and (15) with respect to Equations (16) and (17) are easy to understand. For $\Gamma_{17} = 1$, and $L_{\text{TIR}}$ gives us $\Gamma_{\text{SN}} \approx 0.095 \text{ yr}^{-1}$ and $\Gamma_{\text{SN}} \approx 0.049 \text{ yr}^{-1}$ for M82 and NGC 253, respectively. Thus, the nominal values for $\Gamma_{\text{SN}} = 0.1 \text{ yr}^{-1}$ in Equations (16) and (17), while well in the range of SN rates quoted for both systems (Section 3.3), are larger than those inferred from the total FIR luminosity by a factor of $\sim 1.7$–2.

Note that our estimates of $F_{\text{cal}}$ in Equations (15) and (17) for NGC 253 are still $\sim 5$ times higher than the HESS estimate of $\sim 0.05$, even though we use similar or higher SN rates. The main reason for this is that Acero et al. (2009) assume a GeV–to-TeV spectral slope of 2.1, whereas we use a GeV–to-TeV spectral slope of 1.9.
Table 1
Non-calorimetric Galaxies: Predicted and Observed Gamma-ray Fluxes

| Name         | $D$  | $L_{\mathrm{TIR}}$ | SFR | Calculated $F_{\gamma}$ | Predicted Calorimetric $F_{\gamma}$ | Predicted LTQ $F_{\gamma}$ | Observed $F_{\gamma}$ | $\Sigma_e$ |
|--------------|------|-------------------|-----|-------------------------|-------------------------------------|----------------------------|----------------------|------------|
| LMC          | 0.05 | 8.83              | 0.2 | $1.47 \times 10^{-5}$   | $3.2 \times 10^{-11}$               | $6.2 \times 10^{-11}$      | $(5.7 \pm 1.4) \times 10^{-11}$ | 0.002      |
| SMC          | 0.06 | 7.86              | 0.1 | $5.11 \times 10^{-6}$   | $1.1 \times 10^{-11}$               | $3.1 \times 10^{-11}$      | $10^{-11}$           | 0.003      |
| M31 (NGC 224) | 0.79 | 9.39              | 1.0 | $2.95 \times 10^{-7}$   | $6.4 \times 10^{-13}$               | $6.3 \times 10^{-13}$      | $(2.6 \pm 0.6) \times 10^{-12}$ | 0.004      |
| NGC 598 (M33) | 0.84 | 9.07              | 0.5 | $1.30 \times 10^{-7}$   | $2.8 \times 10^{-11}$               | $5.5 \times 10^{-13}$      | $\lesssim 1.5 \times 10^{-12}$ | 0.002      |
| NGC 6946     | 5.32 | 10.16             | 2.6 | $1.69 \times 10^{-8}$   | $3.7 \times 10^{-12}$               | $1.3 \times 10^{-13}$      | $\ldots$            | 0.004      |
| NGC 5457 (M101) | 6.70 | 10.20            | 1.7 | $6.96 \times 10^{-9}$   | $1.5 \times 10^{-12}$               | $2.9 \times 10^{-14}$      | $\ldots$            | 0.002      |
| NGC 5194 (M51) | 8.63 | 10.42            | 3.6 | $8.89 \times 10^{-9}$   | $1.9 \times 10^{-12}$               | $1.0 \times 10^{-13}$      | $\lesssim 8 \times 10^{-11}$ | 0.006      |
| NGC 3031 (M81) | 3.63 | 9.47              | 0.3 | $4.19 \times 10^{-9}$   | $9.1 \times 10^{-13}$               | $1.3 \times 10^{-14}$      | $\ldots$            | 0.005      |
| NGC 3521     | 6.84 | 9.96              | 0.9 | $3.54 \times 10^{-9}$   | $7.7 \times 10^{-13}$               | $2.5 \times 10^{-14}$      | $\ldots$            | 0.003      |
| NGC 5005     | 7.96 | 10.09             | 1.3 | $3.77 \times 10^{-9}$   | $8.2 \times 10^{-13}$               | $2.3 \times 10^{-14}$      | $\lesssim 8 \times 10^{-11}$ | 0.003      |
| NGC 7331     | 14.71| 10.58             | 5   | $4.25 \times 10^{-9}$   | $9.2 \times 10^{-13}$               | $2.2 \times 10^{-14}$      | $\lesssim 8 \times 10^{-11}$ | 0.002      |

Notes:
- Distances from IRAS BGS unless otherwise noted.
- TIR luminosities from IRAS BGS unless otherwise noted.
- The star formation rate as inferred from the literature. The TIR flux is likely to be inaccurate as a simple SFR indicator at these luminosities (Bell 2003).
- We calculated the bolometric star formation flux from the SFR, using $F_{\mathrm{SF}} = 3.8 \times 10^{-15} \mathrm{erg} \mathrm{cm}^{-2} \mathrm{s}^{-1}$, based on the starburst IR to SFR conversion factor in Kennicutt (1998). See caveats in footnote c.
- We calculated gamma-ray flux predicted in the explicitly calorimetric limit: $F_{\gamma} \left(\mathrm{GeV}\right) = \beta_\gamma F_{\mathrm{SF}} \times 10^{-4} \left(E_{51} n_0 \Psi_{17}\right)$, using $\beta_\gamma = 0.7$ as a fiducial value; see Equation (13).
- We calculated gamma-ray flux predicted by the fiducial model of LTQ, using $F_{\mathrm{LTQ}}$. See solid line in Figure 2. Note that leptonic emission (particularly IC) may dominate at the lowest $\Sigma_e$ and increase the $\gamma$-ray fluxes.
- Measurement of or upper limit on integrated gamma-ray flux of energies $\gtrsim \mathrm{GeV}$.
- Gas surface density. Typical uncertainty in this quantity is $\sim 0.3$ dex.
- Harris & Zaritsky (2009) find an SFR of $0.2 M_\odot$ yr$^{-1}$ in the LMC (as used in Figure 2).
- Calculated using Porter et al. (2009), assuming that $\Gamma = 2.7$ above 1 GeV. Integrating the total emission in Figure 8 of Abdo et al. (2010c) gives similar results.
- Calculated using a total gas mass of $6 \times 10^8 M_\odot$ (Israel 1997) and $R_{25} \approx 4.9$ kpc.
- Harris & Zaritsky (2004) find an average SFR of $0.1 M_\odot$ yr$^{-1}$ in the SMC (as used in Figure 2) over the past few Gyr, with occasional bursts of star formation more recently.
- Calculated from Abdo et al. (2010d), by integrating the total power above 1 GeV plotted in their Figure 5.
- Calculated using a total gas mass of $4.5 \times 10^7 M_\odot$ (Israel 1997) and $R_{25} \approx 3.0$ kpc.
- Williams (2003) find an average SFR of $1 M_\odot$ yr$^{-1}$ in M31 (as used in Figure 2).
- Calculated from the Milky Way-scaled GALPROP model in Figure 2 of Abdo et al. (2010c). See also the upper limit in Blom et al. (1999).
- From Kennicutt (1998). The peak gas surface density compiled in Yin et al. (2009) is comparable.
- Gardan et al. (2007) and references therein find star formation rates of $0.3$ to $2 M_\odot$ yr$^{-1}$ in M33.
- Calculated from Abdo et al. (2010c), scaling from the detection of M31 to the upper limit on M33 for the GALPROP spectral template.
- From Kennicutt (1998).
- This system also has a central dense starburst component with $\Sigma_e \approx 0.04$ g cm$^{-2}$ (Kennicutt 1998), that may be calorimetric, and amounts to $\sim 10\%$ of the total star formation rate.
- Scaled from Leroy et al. (2008) to the distance listed here.
- Calculated from Kennicutt et al. (2008) using the Kennicutt (1998) H$\alpha$ luminosity to SFR conversion.
- This system also has a central dense starburst component with $\Sigma_e \approx 0.06$ g cm$^{-2}$ (Kennicutt 1998), that may be calorimetric, and amounts to $\sim 25\%$ of the total star formation rate.
- EGRET upper limits from Cillis et al. (2005).
- Kennicutt et al. (2008) find an H$\alpha$ luminosity equivalent to $0.5 M_\odot$ yr$^{-1}$, while Davidge (2006) find a star formation rate from 10 to 25 Myr ago (roughly the typical lifetime of GeV CR protons in Milky-Way-like galaxies) of $0.1 M_\odot$ yr$^{-1}$.
- Thilker et al. (2007) compare star formation rates derived through several indicators and find them to be $4.4$ to $6.3 M_\odot$ yr$^{-1}$.

spectral slope of 2.3, derived from the Fermi data. With this spectral slope Acero et al. (2009) effectively underestimate the GeV $\gamma$-ray luminosity of NGC 253 by a factor of $\sim 3$ from 1–220 GeV.

3.3. Primary Uncertainties in $F_{\mathrm{cal}}$

Other $\gamma$-ray sources. Any $\gamma$-ray source besides pionic emission from CR protons lowers our estimate for $F_{\mathrm{cal}}$. Although it is in principle possible that other sources dominate, e.g., the TeV emission, it is likely that the GeV emission is in fact pionic. See Section 4.

Other IR sources. For our main estimates of $F_{\mathrm{cal}}$ in Equations (14) and (15), we have used the total IR light of each galaxy to measure the SFRs of the $\gamma$-ray emitting starbursts. However, in NGC 253 only about half of the IR emission comes from the starburst (Melo et al. 2002). It is also possible that cirrus emission from old stars contributes to the observed IR emission, although we do not expect this to be significant within the starburst itself. Excluding this additional IR light increases the estimates of $F_{\mathrm{cal}}$. Acceleration efficiency. Higher $\eta'$ lowers our estimated $F_{\mathrm{cal}}$. In principle, $\eta'$ can be as high as $\sim 1$ (Ellison & Eichler 1984; Ellison et al. 2004). Efficiencies $\eta' > 1$ are also possible if additional CR power comes from sources other than SNe. We have scaled the above estimates for $F_{\gamma}$ using $\eta' = 0.1$ based on our work on FIR–radio correlation (LTQ; TQW),
which constrains $E_{50} \eta'$ to be $\sim 0.1$, depending on the CR proton injection spectrum (see also Torres et al. 2003; Torres 2004). We emphasize that $\eta'$ is the energy per SN explosion in CR protons with energies $\geq 1$ GeV and does not include low-energy CRs.

### Role of supernovae

Although we have assumed in Equations (16) and (17) (and implicitly assumed in our definition of $\eta'$) that SNe are responsible for all of the CRs, this has not been settled (see Butt 2009). There is evidence now that SN remnants accelerate some CRs (Tavani et al. 2010), but...
other sources may also contribute CRs. The γ-ray detections of M82 and NGC 253, combined with the γ-ray detections of quiescent star-forming galaxies, are evidence that γ-ray emission scales with SFR (Abdo et al. 2010). However, other possible sources of CRs include stellar winds (Quataert & Loeb 2005), superbubbles (Higdon & Lingenfelter 2005; Seaquist & Stanković 2007; Butt & Bykov 2008), pulsars (Arons & Tavani 1994; Bednarek & Protheroe 1997; Bednarek & Bartosik 2004), and gamma-ray bursts (Waxman 1995), which all presumably scale with SFR. It is also possible that the efficiency of some mechanisms, such as superbubble acceleration, is different in starbursts.

 Supernova rates. Even if SNe are responsible for CR acceleration, the SN rates in M82 and NGC 253 are highly uncertain. Estimates of Γ_{SN} come from stellar population fitting (Förster Schreiber et al. 2003), line emission (Bregman et al. 2000; Alonso-Herrero et al. 2003), FIR emission (Mattila & Meikle 2001), comparison of radio sources with models of SN remnants (van Buren & Greenhouse 1994), and direct searches for SNe (Mannucci et al. 2003). Methods based on the bolometric emission are complicated by the star formation history, potential IMF variations in starbursts, including the high-mass (≈8 M☉) slope, the shape of the IMF below ∼1 M☉, and the transition mass between stars that do and do not produce SNe. Each of these numbers can affect Ψ in Equation (13), although we do not expect large variations from galaxy to galaxy (TQW; Persic & Rephaeli 2010).

 Methods that use direct searches for SNe or their remnants are more uncertain, and complicated by biases. For example, many of the radio sources identified as SN remnants in M82 and NGC 253 may be compact H II regions (Seaquist & Stanković 2007). Methods based on the expansion speed of SN remnants may be complicated by different physical conditions in starbursts (Chevalier & Fransson 2001). At present, only two confirmed SNe have been observed in M82 (SN 2004am: Singer et al. 2004; Mattila et al. 2004; SN 2008iz: Brumhuth et al. 2009b, 2010), along with three radio transients over the past ∼30 yr that may be radio SNe (Kronberg & Sramek 1985; Muxlow et al. 1994, 2010). In NGC 253, SN 1940e occurred 53″ (0.9D1.5 kpc) from the galaxy’s center, outside the starburst itself (Kowal & Sargent 1971). No radio SN was observed in NGC 253 over 17 years of observations, but the implied 95% confidence limits on SN rate is weak (≈2.4 yr⁻¹; Lenc & Tingay 2006).

 Overall, Γ_{SN} reported in the literature for M82 and NGC 253 span an order of magnitude, from 0.03 yr⁻¹ to 3 yr⁻¹. Early estimates were very high, with Γ_{SN} ≈ 0.3 yr⁻¹ (Rieke et al. 1980). More recent estimates have revised Γ_{SN} downward to ∼0.1 yr⁻¹ (Muxlow et al. 1994; Huang et al. 1994; van Buren & Greenhouse 1994; Bregman et al. 2000; Förster Schreiber et al. 2001; Mattila & Meikle 2001; Lenc & Tingay 2006; Fenech et al. 2008, 2010). Nonetheless, Γ_{SN} remains uncertain at the factor of ∼2–3 level, and SN rates down to 0.02 yr⁻¹ are possible for both systems (Förster Schreiber et al. 2001; Colina & Perez-Olea 1992; Engelbracht et al. 1998).

 Galaxy distances. The estimates of F_cal in Equations (14) and (15) do not depend on distance because they depend only on the ratio of TIR and γ-ray fluxes.

 Equations (16) and (17) instead assume Γ_{SN}, so that the distances do matter. Models of the γ-ray emission also often assume some distance and SN rate (e.g., Domingo-Santamaría & Torres 2005; LTQ). The estimated distances to NGC 253 vary, from less than 2.3 Mpc (Davidge & Pritchet 1990) to 3.9 Mpc (Karachentsev et al. 2003). This range amounts to an uncertainty of a factor of ∼4 in the γ-ray luminosity of NGC 253. Similarly, distances typically quoted for M82 include 3.3 Mpc (Freedman & Madore 1988), 3.6 ± 0.3 Mpc from Cepheids in M81 (Freedman et al. 1994), and 3.9 ± 0.6 Mpc from the red giant branch (Sakai & Madore 1999), amounting to a ∼40% uncertainty in the luminosity of M82.

 3.4. Assessing Proton Calorimetry

 The values of F_cal derived in Section 3.2 imply efficient proton losses in NGC 253 and M82 compared to the Milky Way. The γ-ray data imply both systems have F_cal ≈ 0.2–0.5 (compared with F_cal < 0.1 in the Milky Way based on grammage estimates and modeling; e.g., Ginzburg & Ptuskin 1976; Garcia-Munoz et al. 1987; Engelmann et al. 1990; Jones et al. 2001; Dogiel et al. 2002; Strong et al. 2010). This suggests that t_π ≈ t_escaped, even though both galaxies exhibit large-scale galactic winds, and that these systems represent the transition to proton calorimetry. The case for calorimetry in M82 is stronger than in NGC 253, although F_cal is uncertain for NGC 253 by a factor of ∼2. If we only use the TIR flux of the core of NGC 253 (about half the total; Melo et al. 2002), F_cal would be about twice as high, or 0.4–0.5—the same as M82 (open star in Figure 2). Thus, the small F_cal for NGC 253 may simply be the result of averaging the γ-rays from the calorimetric starburst with the non-calorimetric outlying disk.

 Figure 2 shows the ratio F_γ(≥ GeV)/F SF (see Tables 1 and 2), the γ-ray flux above 1 GeV to the bolometric flux F_SF produced by young stars, as a function of gas surface density for NGC 253 and M82, as well as for the Large Magellanic Cloud (LMC; Porter et al. 2009), Small Magellanic Cloud (SMC; Abdo et al. 2010d), the Galaxy (Strong et al. 2010), and M31 (Abdo et al. 2010), together with upper limits on M33 from Abdo et al. (2010f) and Arp 220 from our own analysis of the Fermi data (see the Appendix). (Note that the plotted ratio F_γ(≥ GeV)/F SF does not include β_π, since we wish to plot observable quantities.) The dashed line indicates the calorimetric expectation from Equation (13), scaled to η_p = 0.1 and β_π = 0.7, for p = 2.2.

 The solid line is the prediction of the fiducial model of LTQ, derived by combining constraints from the Schmidt Law of star formation and the observed FIR–radio correlation. At low gas surface densities, CR protons easily escape, γ-ray emission is weak and F_cal is small. However, as the gas surface density increases, galaxies become more proton calorimetric and in sufficiently dense starbursts F_cal asymptotes (Equation (13)). For these galaxies we expect an F_γ–γ-ray correlation (TQW). The discontinuity at Σ_g = 0.05 g cm⁻² is due to the transition in scale height from h = 1 kpc (for normal galaxies) to h = 100 pc (starbursts) in the LTQ models; in reality, the transition between normal galaxies and starbursts is smoother. The γ-ray luminosity of the LMC is consistent with the predictions of LTQ to within a factor of ∼2. The standard model of LTQ is tuned to reproduce the Milky Way γ-ray luminosity given

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10 Other estimates include 2.5–2.7 Mpc from de Vaucouleurs (1978), 2.6 Mpc from Puche & Carignan (1988), 2.9 ± 0.5 Mpc from Blecha (1986), 3.3 Mpc from Mouhcine et al. (2005), and 3.5 ± 0.2 Mpc from Rekola et al. (2005). A distance of 2.5 Mpc to NGC 253 is commonly quoted (e.g., Mauersberger et al. 1996b), and is used in the Domingo-Santamaría & Torres (2005) and Rephaeli et al. (2010) models of NGC 253; the HESS analysis similarly used 2.6 Mpc (Acero et al. 2009). TQW and LTQ used 3.5 Mpc, based on the Hubble Law.
in Strong et al. (2000) with \( \Sigma_g = 0.01 \text{ g cm}^{-2} \). A more recent estimate revises the Milky Way pionic \( \gamma \)-ray luminosity down by a factor of \( \sim 3 \) (Strong et al. 2010, hereafter S10); on the other hand, the Milky Way gas surface densities compiled in Yin et al. (2009) are also \( \sim 3 \) times lower (the SFR peaks at \( \sim 6 \text{ kpc} \), where \( \Sigma_g = 0.003 \text{ g cm}^{-2} \)), so that the Galaxy is still fairly close to the LTQ prediction. The SMC is \( \gamma \)-ray dim by a factor of \( \sim 4 \), suggesting that CRs escape much more easily than expected (Abdo et al. 2010d). Similar behavior is indicated for the CR electrons by the radio emission of irregular galaxies (Murphy et al. 2008). However, M31 is surprisingly \( \gamma \)-ray bright with respect to the LTQ prediction. Finally, NGC 253 and M82 appear to be somewhat \( \gamma \)-ray faint compared to LTQ’s fiducial model, consistent with Equations (14) and (15).

A detection of the ULIRG Arp 220 at the level specified in Table 2 would improve our understanding of how \( F_{\text{cal}} \) evolves with \( \Sigma_g \). With average densities in its nuclear starbursts exceeding \( 10^3 \text{ cm}^3 \) (Downes & Solomon 1998), its pionic loss time is less than \( 10^4 \text{ yr} \) (Equation (7)), difficult to reach with winds (Equation (8)). According to the models of LTQ, Arp 220 should not have a significantly larger F, exceeding 104 cm3 (Downes & Solomon 1998), its pionic loss time is less than 104 yr (Equation (7)), difficult to reach with winds (Equation (8)). According to the models of LTQ, Arp 220 should not have a significantly larger F, exceeding 104 cm3 (Downes & Solomon 1998), its pionic loss time is less than 104 yr (Equation (7)), difficult to reach with winds (Equation (8)).

### 4. OTHER SOURCES OF \( \gamma \)-RAY EMISION

Our analysis in Section 3 assumes that the \( \gamma \)-ray emission is primarily pionic. Here, we consider other possibilities that could reduce \( F_{\text{cal}} \).

#### 4.1. Diffuse Leptonic Emission

Primary and secondary CR electrons and positrons (e\(^\pm\)) also contribute to the \( \gamma \)-ray emissivity of M82 and NGC 253 via bremsstrahlung and Inverse Compton (IC) of predominantly dust-reprocessed starlight. Detailed models of M82 and NGC 253 indicate that these emission processes are subdominant for energies more than 200 MeV (Paglione et al. 1996; Domingo-Santamaria & Torres 2005; Persic et al. 2008; de Cea del Pozo et al. 2009a; Rephaeli et al. 2010; de Cea del Pozo et al. 2009b). Even without detailed modeling, these processes almost certainly do not dominate \( L_\gamma \) in the GeV–TeV energy range on energetic grounds. First, more energy goes to \( \pi^0 \rightarrow 2\gamma \) production than to the secondary \( e^\pm \). Second, for a typical ratio of total energy injected in primary electrons to protons of 1/50 (e.g., Warren et al. 2005), and even if all the electron energy goes to producing \( \gamma \)-rays, over 90% (\( F_{\text{cal}} \lesssim 3/50 \)) of the protons would have to escape the starburst for the proton contribution to the \( \gamma \)-ray luminosity to be subdominant. Assuming that none of the protons interact at all, the overall energy budget of the observed \( \gamma \)-ray emission implies that the efficiency of primary electron
acceleration in M82 and NGC 253 would have to be \(~10\) times higher than inferred in the Galaxy. Finally, the magnetic energy density \((B \approx 200 \; \mu G \text{ implying } U_B \approx 1000 \; \text{eV cm}^{-3})\) is predicted to be at least as strong as radiation energy density \((U_{\text{rad}} \approx 200–1000 \; \text{eV cm}^{-3})\;e.g.,\;Paglione \text{ et al.} \;1996; \;Persic \text{ et al.} \;2008; \;\text{in many models (e.g., Condon et al. \;1991; Domingo-Santamaría & Torres \;2005; \;TQW; \;Persic \text{ et al.} \;2008; \;de Cea del Pozo \text{ et al.} \;2009a; \;Rephaeli \text{ et al.} \;2010; \;LTQ.). Thus, synchrotron losses will increase the energetic requirements even further.

However, in specific energy ranges leptonic emission can dominate the \(\gamma\)-ray emissivity. Bremsstrahlung and IC emission probably make up most of the \(\gamma\)-ray emission below 100 MeV (e.g., Paglione \text{ et al.} \;1996; Domingo-Santamaría & Torres \;2005; \;Persic \text{ et al.} \;2008; \;de Cea del Pozo \text{ et al.} \;2009a, \;2009b; \;Rephaeli \text{ et al.} \;2010; \;LTQ). Bremsstrahlung falls off steeply with energy, and is unimportant above \(~\text{GeV})\. The IC spectrum is complicated by the shape of the input photon spectrum. Given that the photon SED of starbursts is dominated by the FIR, for a CR \(e^+\) injection spectrum \(Q(E) \propto E^{-\delta}\), we expect the IC photon index to be \(\Gamma_{\text{IC}} \approx p/2 + 1\) at \(\sim\)TeV energies (Rybicki & Lightman \;1979).\;11\) Whether pionic or advective losses dominate, the pionic emission will have a photon index \(\Gamma_\pi \approx p\); thus, IC can dominate the VHE \(\gamma\)-ray emission, but only if \(p\) is substantially greater than \(2.0\) in the calorimetric or advective limit.\;12\) In practice, Klein–Nishina effects will suppress the IC luminosity beyond a cutoff \(E_{\text{K}\text{N}} \approx 18 \text{ TeV} \; (\lambda /80 \; \mu m )\) for target photons of wavelength \(\lambda\). For these reasons, IC is unlikely to contribute significantly to the TeV emission unless \(p \gtrsim 2.5\).

At present, the \textit{Fermi} detections presented in Abdo \text{ et al.} \;2010a) only use photons with energies greater than 200 MeV. Improving the limits on 100 MeV photons is essential to determining the leptonic contribution, which should begin to dominate at lower energies. Direct detection of bremsstrahlung and IC from electrons and positrons would have strong implications for the synchrotron radio emission, and could test the “high-\(\Sigma\) conspiracy” postulated by LTQ to explain the radio emission of starburst galaxies (see Section 5).

4.2. Discrete \(\gamma\)-ray Sources

Because M82 and NGC 253 are unresolved by \textit{Fermi}, VERITAS, and HESS, the \(\gamma\)-ray detections include diffuse emission from CRs and emission from discrete sources.\;13\) The high-energy particles in these sources responsible for \(\gamma\)-rays need not contribute to the general CR population. Many such sources in the Galaxy are known to be associated with star formation, including pulsars and a large number of unidentified sources (Abdo \text{ et al.} \;2009a), and should be expected in abundance in starbursts.

Because relatively little work has been done on the expected properties of such sources in starbursts, it is unclear if they could dominate the \(\gamma\)-ray emission from M82 and NGC 253. A number of star formation phenomena are known to be TeV sources (as reviewed by, e.g., Grenier \;2008; \;Horns \;2008; \;Hinton & Hofmann \;2009), including SN remnants, PWNe (Abdo \text{ et al.} \;2009b), and possibly star clusters (Aharonian \text{ et al.} \;2007).

The observed Galactic TeV sources tend to have hard spectra \((\Gamma \approx 2.2)\), similar to the observed GeV-to-TeV spectra of M82 and NGC 253.

As an example, PWNe have a total energy budget set by the pulsar rotational energy, \(E_{\text{rot}} \approx 2 \times 10^{50} \; \text{erg} \; P_{0.01}^{-2}\), where \(P_{0.01} = P/0.01 \; \text{s}\) is the pulsar spin period at birth, comparable to that injected into CR protons by the SN remnants. The typical spin-down luminosity is \(E_{\text{rot}} \approx 6 \times 10^{39} P_{0.01}^2 B_{12}^2 \; \text{erg} \; \text{s}^{-1}\), where \(B_{12} = B/10^{12} \; G\) is the pulsar magnetic field strength, corresponding to a spin-down timescale of \(\sim 10^5\) yr. If all of this energy went into \(\gamma\)-ray emission in M82 and NGC 253, a pulsar birth rate of \(~0.1 \; \text{yr}^{-1}\) could easily power the GeV–TeV emission. However, Galactic \(\gamma\)-ray sources like the Crab (e.g., Albert \text{ et al.} \;2008), Geminga (Yüksel \text{ et al.} \;2009), and HESS J1825-137 (Aharonian \text{ et al.} \;2006a) have GeV–TeV luminosities several decades lower than this estimate. For example, the total \(\gamma\)-ray luminosity of the Crab \((L_{\gamma} \approx 10^{35} \; \text{erg} \; \text{s}^{-1})\) implies that \(10^{15}–10^5\) such objects would be needed to contribute significantly to the GeV–TeV emission seen from M82 and NGC 253 (see also Mannheim \text{ et al.} \;2010).

Given the pulsar birthrate and spin-down timescale, this seems unlikely, but we cannot rule out the PWNe in starbursts are much more radiatively efficient in \(\gamma\)-rays than in the Galaxy, for example, through stronger IC losses.

4.3. A TeV Excess?

The TeV background of the Milky Way shows a “TeV excess” above the expected pionic background (Prodanović \text{ et al.} \;2007; \;Abdo \text{ et al.} \;2008). Whether it is caused by unresolved discrete sources or truly diffuse emission is not known; nor is it known whether it is hadronic or leptonic. The TeV excess varies with Galactic latitude, being strongest in the Galactic center and the Cygnus regions (Abdo \text{ et al.} \;2008). The latitude profile of the Galactic TeV \(\gamma\)-ray emission supports a hadronic explanation for the TeV excess, but leptonic models are not yet excluded (Abdo \text{ et al.} \;2008).

The TeV excess is visible in the Galaxy because the pionic spectrum is steep; effectively, the TeV excess changes \(\Gamma\) from 2.7 to 2.6 (Prodanović \text{ et al.} \;2007). If M82 and NGC 253 have hard pionic \(\gamma\)-ray spectra at TeV energies, then the \(\gamma\)-rays from ambient CRs interacting with their ISM will bury any TeV excess. Furthermore, the simplest explanation for a hadronic TeV excess is that some regions of the Galaxy are denser and more proton calorimetric, and that the TeV excess is simply pionic emission from the normal CR protons. This effect is observed in molecular clouds located near CR acceleration sites in the Milky Way (Aharonian \text{ et al.} \;2006b, \;2008; \;Albert \text{ et al.} \;2007), but if \(F_{\text{cal}} \approx 1\), the entire starburst is illuminated this way, and the total pionic \(\gamma\)-ray luminosity cannot be increased further.

5. THE GeV–GHz RATIO: A DIAGNOSTIC OF ELECTRON COOLING AND THE FIR–RADIO CORRELATION

The observed \(\gamma\)-rays from M82 and NGC 253 have important implications for the physics of the radio emission of starburst galaxies (see LTQ and references therein). If pionic, \(L_{\gamma}\) necessarily implies production of secondary \(e^\pm\;s\), which produce synchrotron radiation and contribute to the GHz emissivity of the starbursts. Rengarajan \;2005\;TQW, and LTQ have all argued that secondary \(e^\pm\;s\) dominate the synchrotron emission from

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\(11\) Electrons at these high energies, far greater than those observed at GHz frequencies, are cooled almost entirely by IC and synchrotron.

\(12\) For example, if \(p = 2.2\), then \(\Gamma_{\pi} = 2.2\) and \(\Gamma_{\text{IC}} = 2.1\); over 1 dex in \(\gamma\)-ray energy, this amounts to only a \(\sim 30\%\) increase in the ratio of IC to pionic \(\gamma\)-rays.

\(13\) Emission from active galactic nuclei (AGNs) is unlikely to be important, because no variability is observed (Abdo \text{ et al.} \;2010a) and any AGN luminosity in NGC 253 and M82 is small compared to the star formation luminosity (Brunthaler \text{ et al.} \;2009a).
starbursts. Detailed models of starburst regions by Paglione et al. (1996), Torres (2004), Domingo-Santamaría & Torres (2005), Persic et al. (2008), de Cea del Pozo et al. (2009a), and Rephaeli et al. (2010) find that secondary $e^\pm$ are the majority of $\sim$GeV $e^\pm$, although the number of primary electrons is still within a factor of a few of the secondaries.

The $\gamma$-ray to radio ratio provides an important constraint on the cooling mechanism of GHz-emitting electrons, if the $\gamma$-rays are pionic. This ratio can be understood through a simple argument as follows. Suppose the protons (and secondary $e^\pm$) have an $E^{-2}$ spectrum, with equal energy in each log $E$ bin. The protons lose energy to pions; roughly two times as much energy goes into $\gamma$-rays as electrons and positrons. Furthermore, since $v_c \propto E^{1/2}$, the synchrotron emission from each log bin in $e^\pm$ energy is spread over two log bins in synchrotron frequency. Therefore, if the $\gamma$-ray emission is dominated by diffuse pionic emission, and if the radio emission is dominated by secondary $e^\pm$,

$$v F_v(E_\gamma) = 4 \pi F_v(E_\gamma) f_{\text{syn}},$$  \hspace{1cm} (18)

where $E_\gamma$ and $E_e$ are the energies of $\gamma$-rays and $e^\pm$, respectively, from CR protons of the same energy, and $f_{\text{syn}} = (t_{\text{sync}}/t_{\text{life}})^{-1}$ is the fraction of CR $e^\pm$ power going into synchrotron. CR protons produce pionic $\gamma$-rays with $E_\gamma \approx 0.1 K_p$ and secondary $e^\pm$ with $E_e \approx 0.05 K_p \approx f_{\text{syn}}/2$. Since electrons that emit GHz synchrotron radiation have an energy of $E_{\text{GHz}} \approx 560 \text{MeV} B_{200}^{-1/2} (\nu/\text{GHz})^{1/2}$, we compare $\gamma$-rays and GHz radio emission. The GHz flux of M82 and the starburst core of NGC 253 are 9 and 3 Jy, respectively (Williams & Bower 2010), while the $v F_v(\nu)$ fluxes are $3 \times 10^{-12} \text{erg cm}^{-2} \text{s}^{-1}$ and $2 \times 10^{-12} \text{erg cm}^{-2} \text{s}^{-1}$, respectively. This implies that $f_{\text{sync}}^{-1}$ is $\sim 8$ for M82 and $\sim 17$ for NGC 253, if all of the $\gamma$-ray flux is from their starburst cores. If we instead consider the total GHz-emitting electrons, if the radio emission is dominated by diffuse pionic emission, the fraction of radio emission from primary $e^\pm$, the fraction of $\gamma$-rays and radio from the starburst cores as opposed to the outlying disk galaxies, and the uncertainties in the $\gamma$-ray fluxes.

Bremsstrahlung and ionization can easily provide these extra losses. For $e^\pm$ radiating synchrotron at $v = v_{\text{GHz}}$ GHz, the densities when the bremsstrahlung and ionization cooling timescales are comparable to the synchrotron cooling timescale ($t_{\text{Brems}}/t_{\text{sync}}$ and $t_{\text{ion}}/t_{\text{sync}} \leq 1$) are $n_{\text{eff}} \gtrsim 67 \text{cm}^{-3} v_{\text{GHz}} B_{200}^2$ and $n_{\text{eff}} \gtrsim 54 \text{cm}^{-3}$ $v_{\text{GHz}} B_{200}$, respectively (LTQ; Murphy 2009). These losses are also suggested by the somewhat flattened $\gamma$-ray synchrotron radio spectra observed in starbursts ($\alpha \approx 0.7$), whereas pure synchrotron and IC cooling would lead to steep spectra with $\alpha \approx 1$ (Thompson et al. 2006). Detailed models which do include all of these losses regularly do fit the radio spectra of M82 and NGC 253 (Paglione et al. 1996; Domingo-Santamaría & Torres 2005; Persic et al. 2008; de Cea del Pozo et al. 2009a; Rephaeli et al. 2010) as well as the $\gamma$-ray spectra (de Cea del Pozo et al. 2009b). These models can improve our interpretation of the relevant loss mechanisms. Finally, with more $\gamma$-ray data from Fermi, the lower energy leptonic $\gamma$-ray emission may be detected, which would directly constrain the importance of loss processes such as bremsstrahlung.

6. IMPLICATIONS

A number of previous studies have found implications for $\gamma$-ray bright starbursts. We now discuss these implications in light of the current detections of M82 and NGC 253.

6.1. The Detectability of Other Star-forming Galaxies

Our inference of $F_{\text{cal}} \approx 0.4$ and 0.2 in M82 and NGC 253 implies that a number of local star-forming and starburst galaxies should be visible with next-generation TeV $\gamma$-ray telescopes like the Cherenkov Telescope Array (e.g., Knödlseder 2010) and with additional Fermi data (see also Pavlidou & Fields 2001; Cillis et al. 2005; TQW). For a number of galaxies chosen from the IRAS Bright Galaxy Survey (BGS; Sanders et al. 2003), Tables 1 and 2 list the distance, total FIR luminosity and flux, estimates of the gas surface density $\Sigma_g$, and three determinations of the $\gamma$-ray flux: (1) $F_{\text{cal}}(\gtrsim \text{GeV})$, the purely calorimetric prediction from Equation (13), assuming $\beta_\gamma = 0.7$ and $\Psi_{\gamma\gamma} = 1$, (2) $F_{\gamma}\Psi_{\gamma}\Psi_{\gamma\gamma}(\gtrsim \text{GeV})$, the prediction from LTQ given $\Sigma_g$ and scaled to $F_{\text{TR}}$ (solid line, Figure 2), and (3) the observed flux $F_{\gamma}(\gtrsim \text{GeV})$ in cases where there exists either a detection or an upper limit. Our predictions for $F_{\text{cal}}(\gtrsim \text{GeV})$ use Equation (13) with nominal values of $\beta_\gamma = 0.7$ ($p = 2.2$) and $n' = 0.1$. Tables 1 and 2 provide a useful guide to the
detectability of all local galaxies to the extent that their TIR and γ-ray light are dominated by star formation.

Table 1 provides results for normal star-forming galaxies with low Σγ that are not expected to be calorimetric. Here, \( F_{\gamma}^{\text{cal}}(\geq \text{GeV}) \) provides an upper limit to the pionic γ-ray flux, and \( F_{\gamma}^{\text{LTQ}}(\geq \text{GeV}) \) provides the prediction based on the nominal estimate of \( F(\geq \text{GeV})/F_{\text{IR}} \) for Σγ (solid line, Figure 2) and the SFR listed in the table. Since emission from old stars and different UV opacities can affect the TIR emission (Bell 2003), the γ-ray predictions should be scaled to known SFRs when possible. Furthermore, leptonic processes may increase the γ-ray emission significantly, especially in low-density galaxies. Table 2 gives numbers for the starbursts in the *IRAS BGS*. Here, \( F_{\gamma}^{\text{cal}}(\geq \text{GeV}) \approx F_{\gamma}^{\text{LTQ}}(\geq \text{GeV}) \). Uncertainties in Table 2 include those in the gas surface density Σγ of the starbursts and the fraction of TIR light associated with the denser starburst regions as opposed to the surrounding galaxy in the whole.

Note that if they are in fact calorimetric, the starburst/AGN systems NGC 4945 and NGC 1068 in Table 2 should be the brightest on the sky after M82 and NGC 253 at GeV. We note that Abdo et al. (2010b) very recently announced the γ-ray detection of NGC 4945 (1FGL J1305.4–4928), with a flux within 50% of the calorimetric prediction and very near the LTQ prediction; Lenain et al. (2010) has also announced the detection of NGC 1068. However, it is still uncertain how much of the γ-ray flux from these starbursts is from star formation, and how much is from the Seyfert nuclei (Lenain et al. 2010).

The values in Tables 1 and 2 also should give the approximate neutrino luminosities of nearby starbursts, since charged pions decay into neutrinos (e.g., Stecker 1979). Indeed, models of M82 and NGC 253 predict them to be neutrino sources (e.g., Persic et al. 2008; de Cea del Pozo et al. 2009a; Rephaeli et al. 2008). However, NGC 253 and NGC 4945 as Southern objects are not detectable with IceCube (though they may be detectable with KM3NET; Katz 2006), and M82 is at high declination where IceCube’s sensitivity is the weakest (Abbasi et al. 2009).

6.2. The Diffuse γ-ray and Neutrino Backgrounds from Star Formation

The detections of NGC 253 and M82 at GeV–TeV energies together with our determination of \( F_{\text{cal}} \) in these systems has immediate implications for the diffuse γ-ray and neutrino backgrounds from star formation, as discussed in LW06 and TQW (see also Pavlidou & Fields 2002; Bhattacharya & Sreekumar 2009). Several recent studies present calculations of the star-forming galaxy contribution to the γ-ray background, using the γ-ray brightness of nearby normal galaxies and starbursts, finding contributions of order \( \lesssim 10\%–50\% \) (e.g., Fields et al. 2010; Makiya et al. 2011; Stecker & Venters 2011). Here we present an updated version of TQW’s calculation, based on the IR background and this paper’s \( F_{\text{cal}} \).

The pionic emission from starburst galaxies should be concentrated above 100 MeV, with a power-law spectrum above \( \sim 1 \) GeV to PeV energies if unabsorbed. For an acceleration efficiency of \( \eta' = 0.1 \) (see LTQ), for CR protons energies larger \( \geq \) GeV, the total integrated γ-ray background above 1 GeV is, following Equation (13) and ignoring absorption and redshift effects,

\[
F_{\gamma}(\geq \text{GeV}) \approx 1.0 \times 10^{-6} \eta_{0.1}' f_{\text{burst}} f_{\gamma}^{\text{cal}} F_{\gamma}^{\text{TIR}} \text{GeV s}^{-1} \text{cm}^{-2} \text{sr}^{-1},
\]

for \( \Gamma = 2.2 \), where \( F_{\gamma}^{\text{TIR}} \) is the total diffuse extragalactic TIR background in units of \( 20 \) nW m\(^{-2}\) sr\(^{-1}\), \( f_{\text{burst}}^{\gamma} \) is the fraction of the TIR extragalactic background produced by starburst galaxies (see TQW), and \( F_{\gamma}^{\text{cal}} = F_{\gamma}^{\text{cal}}/0.5 \) is the average calorimetric fraction of these starbursts. As with individual starbursts, the observable neutrino background must be comparable to the pionic γ-ray background, and have a similar spectrum (cf. LW06).

This estimate for the γ-ray and neutrino backgrounds from CR protons implies that for \( E_{\gamma} \gtrsim 1 \) GeV and \( \Gamma = 2.2 \),

\[
\frac{\nu_{\text{CR}}(\text{GeV})}{\nu_{\text{IR}}(\text{GeV})} \approx 2 \times 10^{-3} L_{\text{CR}} L_{\gamma}^{0.2} f_{\text{burst}} f_{\gamma}^{\text{cal}} F_{\gamma}^{\text{TIR}} \text{GeV}^{0.5} \text{cm}^{-2} \text{sr}^{-1},
\]

where \( f_{\text{burst}}^{\gamma} \) is the fraction of the TIR extragalactic background produced by starburst galaxies (see TQW), and \( F_{\gamma}^{\text{cal}} = F_{\gamma}^{\text{cal}}/0.5 \) is the average calorimetric fraction of these starbursts. As with individual starbursts, the observable neutrino background must be comparable to the pionic γ-ray background, and have a similar spectrum (cf. LW06).

6.3. The Dynamical Importance of Cosmic Rays in Starbursts

CRs are dynamically important with respect to gravity in the Galaxy (Boulares & Cox 1990). They have recently been claimed to be subdominant with respect to gravity in starbursts because of strong pion losses (LTQ). However, CRs may be important in driving winds in such systems (Socrates et al. 2008), as in the Galaxy (Chevalier & Fransson 1984; Everett et al. 2008). The observed γ-ray emission from M82 and NGC 253 may be converted into a constraint on the product of \( n_{\pi} \) (see Equation (7)) and the energy density of the CRs, \( U_{\text{CR}} \), and hence inform the question of whether or not CRs are dynamically important in these systems:

\[
L_{\gamma}(K_{\text{CR}} \geq \text{GeV}) \approx U_{\gamma} V f_{\text{GeV}}/L_{\gamma},
\]

where \( L_{\gamma}(K_{\text{CR}} \geq \text{GeV}) \approx 3 \beta_{\gamma}^{-1} L_{\gamma}(\geq \text{GeV}) \), \( V \) is the starburst volume, and \( f_{\text{GeV}} \) is the fraction of the CR energy density in CRs with energy above 1 GeV. Taking values for the radius and scale height of \( R_{250} = R/250 \) and \( h_{100} = h/100 \) pc,

\[
U_{\text{CR}n_{\pi}} \approx 6100 \text{ eV cm}^{-6} f_{\text{GeV}}^{1.5} R_{250}^{-1} h_{100}^{-1} D_{1.5}^{-2} \beta_{\gamma}^{-1} N^{-0.9}.
\]
If we assume \( R_{250} = h_{100} = 1 \) and that CRs interact with an average density of \( \sim 250 \text{ cm}^{-3} \), then \( U_{\text{CR}} \sim 300 f^{-1}_{\text{GeV}} \text{ eV cm}^{-3} \) for M82 (comparable with Acciari et al. 2009) and \( \sim 100 f^{-1}_{\text{GeV}} \text{ eV cm}^{-3} \) for NGC 253 (extrapolating to 1.3 TeV). 12 eV cm\(^{-3}\), about twice that of Acero et al. 2009; however, they quote \( n_{\text{eff}} \approx 600 \text{ cm}^{-3} \). For a \( K^{-1.3} \) CR spectrum stretching from 10 MeV to infinity (Torres 2004), \( f_{\text{GeV}} \approx 0.25 \), mostly in low (\( \ll \text{GeV} \)) energy CRs. 15 Although the thermal pressure within M82 is an order of magnitude less for M82 (comparable with Acciari et al. 2009) and \( \sim 250 \text{ cm}^{-3} \), about twice that of Acero et al. 2009; however, they quote \( n_{\text{eff}} \approx 600 \text{ cm}^{-3} \). For a \( K^{-1.3} \) CR spectrum stretching from 10 MeV to infinity (Torres 2004), \( f_{\text{GeV}} \approx 0.25 \), mostly in low (\( \ll \text{GeV} \)) energy CRs. 15

There is a degeneracy between \( U_{\text{CR}} \) and \( n_{\text{eff}} \); at fixed \( L_{\gamma} \), a small \( n_{\text{eff}} \) can be accommodated by having a high \( U_{\text{CR}} \), and vice versa. The value of \( n_{\text{eff}} \) is not obvious since the ISM of starbursts is highly turbulent and clumpy, with most of the volume filled with gas that is underdense with respect to the mean density. The pressure required for hydrostatic balance is \( P_{\text{hydro}} \approx \pi G \Sigma \Sigma_{\text{tot}} \), where \( \Sigma_{\text{tot}} \) is the total surface density and is approximately equal to \( \Sigma_{\text{e}} \). 15 We find that the CR pressure \( P_{\text{CR}} = U_{\text{CR}}/3 \) is dynamically unimportant: \( P_{\text{CR}} / P_{\text{hydro}} \approx 0.02 f^{-1}_{\text{GeV}} \). Alternatively, if we assume that \( P_{\text{CR}} \approx P_{\text{hydro}} \), we find that \( n_{\text{eff}} \approx 0.02 f^{-1}_{\text{GeV}} (n) \approx 5-20 \text{ cm}^{-3} \), implying that \( \tau_{\gamma} \approx 5 \text{ Myr} \), approximately 25 times longer than the nominal wind escape timescale (see Equation (8)). This requires far more efficient CR acceleration than \( \eta' \approx 0.1 \) (see Section 3.2), which we consider unlikely. Therefore, we conclude that \( P_{\text{CR}} \ll P_{\text{hydro}} \).

7. CONCLUSION

M82 and NGC 253 have now been detected in GeV and TeV \( \gamma \)-rays, with fluxes roughly comparable to previous detailed predictions. We have shown that the observed \( \gamma \)-ray fluxes imply that a fraction \( F_{\text{cal}} \approx 0.2-0.4 \) of the energy injected into high-energy CR protons is lost to inelastic collisions (pion production) with protons in the ISM (for \( \eta' = 0.1 \)). However, \( F_{\text{cal}} \) in the range of 0.1–1 can be accommodated with different SNe rates and acceleration efficiencies (see the uncertainties in Sections 3.3 and 4). We find a significantly higher \( F_{\text{cal}} \) for NGC 253 than Acero et al. (2009) because NGC 253 has more GeV emission than they expected. The uncertainty in \( F_{\text{cal}} \) will decrease significantly with more observations by Fermi, HESS, and VERITAS.

A future test of proton calorimetry in M82 and NGC 253 would be a \( \gamma \)-ray detection of a ULIRG like Arp 220 (cf. Torres 2004). Arp 220 is more likely to be a proton calorimeter than M82 and NGC 253, with its extremely high average gas density. If M82 and NGC 253 are not proton calorimeters but Arp 220 is, the ratio of Arp 220’s pionic luminosity to its stellar luminosity will be greater than M82 and NGC 253—it will be brighter in \( \gamma \)-rays than expected (see Figure 2, Tables 1 and 2). Unfortunately, Arp 220’s flux is expected to be challenging to detect with Fermi, although upper limits alone may be constraining (as in the Appendix). Stacking searches of ULIRGs may also prove useful.

Pionic \( \gamma \)-ray emission implies secondary \( e^{\pm} \) production in these starbursts (cf. Rengarajan 2005); from the GHz to GeV ratio, we found evidence of significant non-synchrotron losses. This suggests that bremsstrahlung and ionization are important energy loss mechanisms for CR electrons and positrons (cf. Murphy 2009). This would support the idea presented in Thompson et al. (2006) that these losses flatten the GHz radio spectrum of starbursts (Section 5). It would also support the “high-\( \Sigma_{\text{e}} \) conspiracy” suggested by LTQ to explain the linearity of the FIR–radio correlation for starbursts, whereby bremsstrahlung, ionization, and IC losses suppress the synchrotron radio emission of CR electrons in starbursts, but proton calorimetry leads to secondary electrons and positrons that boost the radio emission.

Whatever the underlying physics of \( \gamma \)-ray production in M82 and NGC 253 is, the high fluxes of these starbursts suggest that other starbursts should also be \( \gamma \)-ray sources. We compile our predictions in Tables 1 and 2. Considering that much of the star formation in the universe at high-\( z \) is in luminous IR galaxies (e.g., Elbaz et al. 1999; Chary & Elbaz 2001; Pérez-González et al. 2005; Magnelli et al. 2009), starbursts might make up a significant fraction (\( \sim 1/2 \)) of the entire \( \gamma \)-ray background (e.g., Pavlidou & Fields 2002; TQW, Bhattacharya & Sreekumar 2009; Section 6.2). If the hadronic interpretation of the \( \gamma \)-ray flux holds, the neutrino background should also be large (LW06).

Finally, the conclusion that M82 has \( F_{\text{cal}} \approx 0.4 \) and NGC 253 has \( F_{\text{cal}} \approx 0.2 \) implies that the pion cooling timescale is nearly equal to the wind escape timescale, \( \sim 2 \times 10^{5} \text{ yr} \) for these systems. This, in turn, suggests that the CR protons on average interact with ISM near the mean density. If this is correct, then the CR pressure is significantly below the pressure needed to support each starburst gravitationally, and CRs are not on average dynamically important deep within the starbursts (Section 6.3).

We thank Matthew Kisler, Boaz Katz, and especially John Beacom for many useful discussions. B.C.L. is supported in part by an Elizabeth Clay Howald Presidential Fellowship. T.A.T. is supported in part by an Alfred P. Sloan Fellowship. This work is funded in part by NASA ATP grant NNX10AD01G. E.Q. was supported in part by NASA grant NN06GI68G, the David and Lucile Packard Foundation, and the Miller Institute for Basic Research in Science, University of California Berkeley. A.L. was supported in part by NSF grant AST-0907890, and by NASA grants NNA09DB30A and NNX08AL43G. E.W.’s research is partially supported by ISF and AEC grants. This research has made use of the NASA/IPAC Extragalactic Database (NED) which is operated by the Jet Propulsion Laboratory, California Institute of Technology, under contract with the National Aeronautics and Space Administration.

APPENDIX

FERMI DATA ANALYSIS FOR Arp 220

We followed the procedure of Abdo et al. (2009a), using the publicly available Fermi data reduction software. The analysis is reviewed in the available online documentation.16 We downloaded data from the Fermi LAT data server17 for METs of 239557417 to 286813463, a total of 18 months. Data from within 20° of each source were downloaded. We created an exposure cube for the entire sky for this time range. We first divided the Fermi energy range into two broad bands: a low-energy bin for 100 MeV \( \leq E_{\gamma} \leq 1 \text{ GeV} \) and a high-energy bin for 1 GeV \( \leq E_{\gamma} \leq 100 \text{ GeV} \). The source region had a radius of 10°. The selection was done with gtselect. We then selected high-quality events with gtmktime.

15 Although the thermal pressure within M82 is an order of magnitude less than \( P_{\text{hydro}} \) (Lord et al. 1996; Smith et al. 2006), the turbulent pressure is comparable to \( P_{\text{hydro}} \) (Smith et al. 2006).

16 Located at http://fermi.gsfc.nasa.gov/ssc/data/analysis/documentation/; the unbinned likelihood tutorial, which we followed, is specifically at http://fermi.gsfc.nasa.gov/ssc/data/analysis/scitools/likelihood_tutorial.html.

17 Available at http://fermi.gsfc.nasa.gov/ssc/data/.
Using the exposure cube, we created an exposure map around each source using gtextmap. Finally, we could perform an unbinned likelihood analysis with glike. We modeled all of the sources listed in the 1FGL Fermi source catalog within 15° of Arp 220, the extragalactic background, diffuse Galactic emission, and Arp 220 itself. In each energy band, we fit a power law to all of the point sources, including Arp 220; both differential flux and integrated flux were considered for Arp 220. We used the P6_V3_DIFFUSE response function. The Galactic background was modeled with the gll_iem_v02.fit background and the extragalactic background was modeled with isotropic_iem_v02.txt, both of which are the default models. We first found a preliminary fit using DRMNFB, and then used the results of that fit to converge to our final fit with MINUIT. We did not detect Arp 220, as expected. Our results are summarized in Table 3. For the high-energy band, we considered both models where $\Gamma$ for Arp 220 was allowed to vary, and models where it was forced to 2.2. In the former, $\Gamma$ always was forced to its maximum value of 5.0, possibly because of a dearth of high-energy photons. Both variants give similar results for the integrated number of photons above 1 GeV, but in the $\Gamma \rightarrow 5$ model, the normalization of the differential flux at 1 GeV is much higher.

### Table 3

| Property | Value |
|----------|-------|
| $100 \text{ MeV} - \text{GeV}$ | $10^4 \text{ ph cm}^{-2} \text{s}^{-1}$ |
| $\Phi_{100}^{\text{int}}$ | $(1.4 \pm 0.5) \times 10^{-9} \text{ ph cm}^{-2} \text{s}^{-1}$ |
| $\Gamma_{100}^{\text{int}}$ | $1.7 \pm 0.4$ |
| $\sqrt{\text{TS}_{100}^{\text{int}}}$ | 0.74 |
| $\Lambda(100 \text{ MeV})$ | $(16 \pm 8) \times 10^{-9} \text{ ph cm}^{-2} \text{s}^{-1} \text{GeV}^{-1}$ |
| $\Phi_{100}^{\text{int}}$ | $(0.30 \pm 0.05) \times 10^{-9} \text{ ph cm}^{-2} \text{s}^{-1}$ |
| $\Gamma_{100}^{\text{int}}$ | $1.2 \pm 0.7$ |
| $\sqrt{\text{TS}_{100}^{\text{int}}}$ | 0.74 |
| $\Lambda(100 \text{ MeV})$ | $(1.2 \pm 0.7) \times 10^{-9} \text{ ph cm}^{-2} \text{s}^{-1} \text{GeV}^{-1}$ |
| $\Phi_{100}^{\text{int}}$ | $(0.24 \pm 0.17) \times 10^{-9} \text{ ph cm}^{-2} \text{s}^{-1}$ |
| $\Gamma_{100}^{\text{int}}$ | $1.7$ |
| $\sqrt{\text{TS}_{100}^{\text{int}}}$ | 1.7 |
| $\Lambda(100 \text{ MeV})$ | $(0.24 \pm 0.17) \times 10^{-9} \text{ ph cm}^{-2} \text{s}^{-1} \text{GeV}^{-1}$ |

**Notes.**

- a Best-fit integrated flux from 100 MeV to 1 GeV.
- b Best-fit photon index between 100 MeV and 1 GeV.
- c Test statistic for power-law fit between 100 MeV and 1 GeV for Arp 220; the square root is roughly the significance of detection.
- d Best-fit differential flux at 100 MeV.
- e Integrated flux from 1 GeV to 100 GeV.
- f Best-fit photon index between 1 GeV and 100 GeV.
- g The best-fit model for Arp 220 has a $\Gamma$ of 5.0, which was the maximum allowed by our source model file. This is why the differential flux seems large when the integral flux is small compared to the maximum allowed by our source model file. This is why the square root is roughly the significance of detection.
- h Best-fit differential flux at 1 GeV.
