THE INFRARED SPECTRAL ENERGY DISTRIBUTION OF NORMAL STAR-FORMING GALAXIES: CALIBRATION AT FAR-INFRARED AND SUBMILLIMETER WAVELENGTHS

Daniel A. Dale
Department of Physics and Astronomy, University of Wyoming, Laramie, WY 82071

AND

George Helou
Infrared Processing and Analysis Center, California Institute of Technology, MS 100-22, 770 South Wilson Avenue, Pasadena, CA 91125

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ABSTRACT

New far-infrared and submillimeter data are used to solidify and to extend to long wavelengths the empirical calibration of the infrared spectral energy distribution (SED) of normal star-forming galaxies. As was found by Dale and coworkers in 2001, a single parameter family, characterized by $f_\nu(60 \mu m)/f_\nu(100 \mu m)$, is adequate to describe the range of normal galaxy SEDs observed by the Infrared Astronomical Satellite and Infrared Space Observatory from 3 to 100 $\mu m$. However, predictions based on the first-generation models at longer wavelengths (122–850 $\mu m$) are increasingly overluminous compared to the data for smaller $f_\nu(60 \mu m)/f_\nu(100 \mu m)$, or alternatively, for weaker global interstellar radiation fields. After slightly modifying the far-infrared/submillimeter dust emissivity in those models as a function of the radiation field intensity to better match the long-wavelength data, a suite of SEDs from 3 $\mu m$ to 20 cm in wavelength is presented. Results from relevant applications are also discussed, including submillimeter-based photometric redshift indicators, the infrared energy budget and simple formulae for recovering the bolometric infrared luminosity, and dust mass estimates in galaxies. Regarding the latter, since galaxy infrared SEDs are not well described by single blackbody curves, the usual methods of estimating dust masses can be grossly inadequate. The improved model presented herein is used to provide a more accurate relation between infrared luminosity and dust mass.

Subject headings: dust, extinction — galaxies: general — galaxies: ISM — infrared: galaxies — infrared: ISM

On-line material: color figures

1. INTRODUCTION

A new model for the infrared spectral energy distribution (SED) of star-forming galaxies, based primarily on Infrared Astronomical Satellite (IRAS) and Infrared Space Observatory (ISO) observations of 69 normal galaxies (Dale et al. 2000), was developed by Dale et al. (2001). A particularly useful feature of these models is that the various SED shapes are adequately described by a single-parameter family, namely, depending only on $f_\nu(60 \mu m)/f_\nu(100 \mu m)$, the ratio of the two far-infrared flux densities measured by IRAS and an indicator of the typical dust-grain temperature; the full suite of galaxy infrared SEDs can be described as spanning a range of far-infrared colors and thus dust temperatures. However, although they span a large wavelength range, 3–1000 $\mu m$, the model curves were constrained using data only from 3–100 $\mu m$. This dearth of far-infrared and submillimeter data for normal star-forming galaxies is largely a consequence of prior instrumental limitations: IRAS did not probe beyond 100 $\mu m$, and the first-generation submillimeter instruments for continuum observations were single-channel broadband photometers, making it difficult to generate spatial maps of cold dust in large nearby galaxies.

Fortunately, with the opportunities provided by ISO and the advent of sensitive submillimeter detector arrays, there are now substantial far-infrared and submillimeter databases for normal star-forming galaxies. For example, Dunne et al. (2000b) and Dunne & Eales (2001) have used the Submillimeter Common-User Bolometric Array (SCUBA) to systematically map 114 galaxies from the IRAS Bright Galaxy Sample (Soifer et al. 1989) at 450 and 850 $\mu m$. Furthermore, a template for the far-infrared continuum of galaxies is being constructed and is based on ISO Long-Wavelength Spectrometer (ISOLWS) continuum data for 228 galaxies at 52, 57, 63, 88, 122, 145, 158, and 170 $\mu m$ (Brauher 2002). In addition, Stickel et al. (2000) provide 170 $\mu m$ data from the ISOPHOT Serendipity Survey for 115 galaxies. We use these data to constrain our SED model beyond 100 $\mu m$.

Infrared continuum data are frequently used to estimate the dust mass of galaxies. However, these calculations typically assume that the infrared emission arises from a single-temperature blackbody. Surely, the integrated infrared emission from galaxies stems from dust spanning a wide range of temperatures. In fact, some of the dust emission is not even from dust in thermal equilibrium; polycyclic aromatic hydrocarbons (PAHs) and very small grains are stochastically heated (Draine & Li 2001). How do the “true” dust masses for the model SEDs compare with those derived from the canonical single-temperature blackbody approach? As is shown below, the standard approach severely underestimates galaxy dust masses.

2. A PHENOMENOLOGICAL MODEL FOR THE INFRARED SPECTRAL ENERGY DISTRIBUTIONS

Désert, Boulanger, & Puget (1990) developed infrared SEDs appropriate for dust emission from individual regions
within the Milky Way. Their models were based on three dust components: large “classical” grains that are in thermal equilibrium, semistochastically heated “very small grains,” and two-dimensional PAHs stochastically heated by individual ultraviolet or optical photons. Starting from the framework laid out by Désert et al. (1990) for Milky Way dust emission, Dale et al. (2001) constructed a wide range of semiempirical infrared SEDs, with the shape and normalization of each determined by the intensity $U$ of the interstellar radiation field, normalized such that $U = 1$ for the local interstellar radiation field; the models span $0.3 \leq U \leq 10^5$. They reasoned that since the integrated emission from normal galaxies results from a superposition of emission from these various environments, it is reasonable to compute “global” spectra from a power-law distribution of the local SEDs. The local SEDs are combined assuming a power-law distribution of dust mass over heating intensity in a given galaxy,

$$dM_d(U) \propto U^{-\alpha} dU,$$

where $M_d(U)$ is the dust mass heated by a radiation field at intensity $U$ and the exponent $\alpha$ is a parameter that represents the relative contributions of the different local SEDs.

The SED model of Dale et al. (2001) was constrained by IRAS and ISOCAM broadband photometric and ISO-PHOT spectrophotometric observations of a sample of 69 normal star-forming galaxies between 3 and 100 $\mu$m ($L_{\text{FIR}}$ from less than $10^8 L_\odot$ to as large as $10^{12} L_\odot$). The model reproduces well the empirical spectra and infrared color trends; the range of $\alpha$ that describes the suite of normal galaxy SEDs is approximately $1 \leq \alpha \leq 2.5$. A power-law distribution model for the radiation field was also successfully applied to the Small Magellanic Cloud SED (Li & Draine 2002). Interestingly, power-law profiles with similar exponents are found for the mass distributions of clouds in the interstellar medium (Stutzki 2001; Shirley et al. 2002; Elmegreen 2002).

3. COMPARISON OF PREVIOUS MODEL WITH LONG-WAVELENGTH DATA

3.1. Comparison with SCUBA 850 $\mu$m Observations

Figure 1 shows a comparison of observed SCUBA 850 $\mu$m fluxes for 110 galaxies (Dunne et al. 2000b) with the 850 $\mu$m fluxes predicted from the suite of SED models Dale et al. (2001) derived for normal star-forming galaxies. For each SCUBA source, a corresponding SED model is selected solely according to $f_{\nu}(60 \mu m)/f_{\nu}(100 \mu m)$. Then, an 850 $\mu$m model flux is generated by convolving the model SED with the SCUBA 850 $\mu$m filter and atmospheric transmissivity profiles. No trend is seen as a function of far-infrared flux and luminosity, but a clear trend is seen with far-infrared color: the model prediction is increasingly overluminous at 850 $\mu$m for progressively cooler galaxies. Moreover, the average model is overluminous by a factor of 2. One potential explanation would be an overestimation of dust emissivity at long wavelengths, which is an unconstrained parameter.

Are similar trends seen within galaxies? This question is unfortunately difficult to answer, since there are very few complete submillimeter maps of large nearby galaxies, in which the large angular extent of the dust emission allows several spatially independent pointings. Bianchi et al. (2000) have obtained such a map for NGC 6946. Using their submillimeter data, a model bias similar to that seen in Figure 1 is found within the disk of NGC 6946.

3.2. Comparison with ISO Far-Infrared Spectroscopy and Photometry

The archival ISOLWS work of Brauher (2002) provides a useful resource for checking the far-infrared continuum levels of the SED model. Part of his study concentrates on measuring galaxy far-infrared continuum levels at 52, 57, 63, 88, 122, 145, 158, and 170 $\mu$m based on ISOLWS data for 228 galaxies (183 of which are unresolved by the ISOLWS beam). After fitting and subtracting any line emis-

Fig. 1. — Comparison of observed SCUBA 850 $\mu$m fluxes (Dunne et al. 2000a) with the 850 $\mu$m fluxes predicted from the SED model of Dale et al. (2001). Here the luminosity at 60 $\mu$m is defined as $4\pi d^2 f_{\nu}(60 \mu m)$, where $d$ is the distance to the galaxy in the Local Group rest frame.
Brauher gauges the baseline continuum level detected by ISO over a 2–5 μm wide spectral window centered on each line wavelength.

Each of the galaxies studied by Brauher (2002) was detected by IRAS at 60 and 100 μm. Since the models are parameterized by $f_\nu(60 \mu m)/f_\nu(100 \mu m)$, the particular SED shape selected for each galaxy is based solely on the observed far-infrared color. The predicted continuum level at each line wavelength is then scaled by the observed IRAS flux density [the result is independent of whether $f_\nu(60 \mu m)$ or $f_\nu(100 \mu m)$ is used]. Figure 2 displays a comparison between the far-infrared continuum levels observed by ISOLWS (open circles) and those predicted by the models. The outliers are the fainter galaxies with low (or possibly even nondetected) continuum levels that are particularly affected by any errors in dark current–subtraction (as large as 10 Jy for some observations) and perhaps light leaks (J. Brauher 2001, private communication). Also portrayed in Figure 2 is a comparison involving the 170 μm continuum levels from the ISOPHOT Serendipity Survey (Stickel et al. 2000). The trend is similar to what is seen using the 170 μm data of Brauher (2002) and is in the same sense as the trend at 850 μm: the models are overluminous for the coldest galaxies, yet become progressively underluminous for galaxies with increasingly blue far-infrared colors.

If the colder galaxies in the Stickel et al. and Brauher samples subtend sizes larger than the instrument fields of view, and conversely, if the hotter galaxies are compact enough to fit within the beams, then the observed trends could result. As stated above, 45 of the 228 galaxies from the Brauher study are resolved by ISOLWS, and thus the observed continuum fluxes may be underestimated because of missing flux from the galaxy outskirts. However, this is unlikely to be a major concern for these galaxies, since the 60 and 100 μm fluxes extracted from the ISOLWS spectra agree with the global IRAS fluxes to within 5%. The trend in the data from the Serendipity Survey is likely not a remnant of beam-size effects or their data reduction techniques, since the envelope of their photometric data agrees with the envelope of Brauher’s spectroscopic data. Moreover, the ISOPHOT data from Stickel et al. derive from a much larger beam than the Brauher ISOLWS data. The best agreement between the far-infrared observations and the models holds for $\lambda < 100 \mu m$, but this is not surprising, given that the SED model of Dale et al. (2001) was based on existing data from 3 to 100 μm. The combination of good agreement at $\lambda < 100 \mu m$ and increasing overestimation at longer wavelengths again points to a possible overestimation of dust emissivity at longer wavelengths.

4. AN IMPROVED DESCRIPTION OF DUST EMISSIVITY

4.1. Evidence for Variations in Dust Emissivity

An important factor in modeling the far-infrared emission from dust is the emissivity index $\beta$, a parameter that

![Figure 2](image_url)
relates a dust grain’s emissivity to the wavelength of emission: \( \epsilon_{\nu} \propto \nu^{-\beta} \). Typical reported values for dust emissivity range from \( \beta = 1 \) to 2, but anecdotal evidence supports an emissivity parameter that depends on environment and that may reach more extreme values. One line of evidence for an environmentally sensitive \( \beta \) comes from the Dunne et al. (2000b) SCUBA data: \( \beta \) appears to decrease with increasing dust temperature \( T_{\text{dust}} \). Additional 850 \( \mu m \) SCUBA data imply that \( \beta \sim 1 \) for luminous infrared galaxies with higher infrared-to-blue ratios (see Fig. 2 of Lisenfeld, Isaak, & Hills 2000). On the other hand, balloon-based submillimeter observations of interstellar clouds indicate that \( \beta \) can reach quite large values. Data from the Polaris flare and of a translucent filament in the Taurus molecular complex show that \( \beta = 1.9–2.2 \) for extremely cold (12–13 K) dust (Bernard et al. 1999; Stepnik et al. 2001). Recent findings by Dupac et al. (2001) support these claims. They find from similar balloon-based submillimeter observations of Orion and M17 molecular cloud regions that \( \beta \) varies from 1 to 2.5 and is anticorrelated with the local dust temperature: the larger values correspond to the colder locales (\( \sim 15 \) K). Furthermore, star counts toward Polaris and Taurus suggest that the cold dust component far-infrared/submillimeter emissivity is about 3 times higher than for the warm dust (Cambresy et al. 2001; Stepnik et al. 2001).

Finally, work by Pollack et al. (1994) shows that \( \beta \) can be as large as 2.5 in the far-infrared/submillimeter for molecular clouds and accretion disks but may drop to near zero at longer (millimeter) wavelengths. Clearly, there is a growing body of observational evidence that \( \beta \) can vary substantially and that it is correlated with the characteristics of the overall local environment.

Laboratory studies also indirectly point to a similar scenario. Work on different amorphous silicates in the submillimeter/millimeter wavelength range shows that \( \beta \) ranges from 1.2 to 2.7 (Agladze et al. 1996) and is anticorrelated with dust temperature. This trend holds down to \( T_{\text{dust}} \sim 10 \) K, but Agladze et al. did not probe to wavelengths shorter than the submillimeter. Menella et al. (1998), however, did study crystalline and amorphous grains from 20 \( \mu m \) to 2 mm, and they found a similar anti-correlation, over a temperature range \( T_{\text{dust}} = 24–295 \) K.

### 4.2. Variable Dust Emissivity Model

In the original work of Désert et al. (1990) and in that continued in Dale et al. (2001), large grains are responsible for the bulk of the far-infrared emission of galaxies. The far-infrared emissivity of this material was assumed to follow an index \( \beta = 1.5 \) for \( 20 \mu m < \lambda < 100 \mu m \) and \( \beta = 2.0 \) beyond 100 \( \mu m \). In keeping with the philosophy that infrared SED shapes are to first order a function of \( U \) (or equivalently, \( f_{\nu}(60 \mu m)/f_{\nu}(100 \mu m) \)), we correct for the residuals in Figure 1 according to \( U \). One such remedy is to alter the large-grain dust emissivity parameter:

\[
\beta = 2.5 - 0.4 \log U .
\]  

Since previously the SED model was empirically calibrated with data at \( \lambda < 100 \mu m \), this new modification is only invoked for \( \lambda > 100 \mu m \). This relation generally follows the trend suggested by the data: \( \beta \) increases (dust emissivity decreases) as the heating intensity decreases. For \( U = 1, 10, \) and 1000, the index is \( \beta = 2.5, 2.1, \) and 1.3, respectively. Figure 3 displays the large-grain emission profiles for the range \( U = 0.3 - 10^3 \), and Figure 4 gives the resulting model-data residuals at 850 \( \mu m \). Equation (2) was selected based on a simple optimization criterion: it minimizes the model-data residuals. Note that in addition to having removed the obvious trend with \( f_{\nu}(60 \mu m)/f_{\nu}(100 \mu m) \), there continue to be no significant trends as a function of flux and luminosity, and the overall ratio means are now centered on unity. The slope of the linear fit to the residuals in the left panel has dropped from 1.23 to 0.39 (see also Fig. 1, Table 1).

The far-infrared residuals portrayed in Figure 2 also decrease after invoking the variable dust emissivity index prescribed in equation (2). The trends in the far-infrared residuals can essentially be completely removed with a more drastically variable dust emissivity index, \( \beta = 2.8 - 0.8 \log U \), but then this overcompensates for the initial trend seen at 850 \( \mu m \). Given that the 850 \( \mu m \) data are more reliable, we proceed with the prescription outlined by equation (2). The relative improvement in the far-infrared residuals is described in Table 1. The improvement is larger at longer wavelengths because the change in dust emissivity is only applicable for \( \lambda > 100 \mu m \); the trends change a bit for \( \lambda < 100 \mu m \), since the predicted \( IRAS \) 100 \( \mu m \) fluxes are slightly different, and thus predictions of the model based on \( f_{\nu}(60 \mu m)/f_{\nu}(100 \mu m) \) are slightly influenced.

### 5. RESULTS

#### 5.1. Presentation of New SEDs

Figure 5 shows the updated infrared SEDs. As portrayed in the bottom panel of Figure 5, the curves have also been extended to radio wavelengths. The extension relies on the well-known far-infrared–to–radio correlation for galaxies: \( q = \log \left( \text{FIR}/3.75 \times 10^{12} \text{ Hz}/f_{\nu}(1.4 \text{ GHz}) \right) \), where “FIR” is the \( IRAS \)-based definition for the 42–122 \( \mu m \) far-infrared flux (see Helou, Soifer, & Rowan-Robinson 1985; Helou et
A recent analysis of IRAS and radio continuum data for 1809 galaxies by Yun, Reddy, & Condon (2001) gives $q \approx 2.34 \pm 0.01$, with a 1$\sigma$ dispersion of 0.26 dex. The model SEDs assume a constant ratio $q$, as there is no correlation with either far-infrared color or luminosity (Yun et al. 2001; M. Yun 2002, private communication). The radio flux arises from two general components: nonthermal processes such as synchrotron radiation resulting from the interaction of supernova-generated cosmic rays and interstellar magnetic fields, and thermal free-free emission from ionized gas (Helou & Bicay 1993). As outlined by Condon (1992), the thermal fraction of the flux density at 20 cm in normal star-forming galaxies is about 10% and exhibits a rather flat spectral slope of $f_{\nu,\text{th}} / f_{\nu,\text{th}}^{-0.1}$; 90% is nonthermal, and typically $f_{\nu,\text{th}}^{-0.8}$. These fractions and spectral indices are employed in the model.

### 5.2. Improving upon Standard Dust Mass Estimations

The large dust grains in normal galaxies are assumed to be in thermal equilibrium, and thus the dust mass can be computed for a given flux density $f_{\nu}$ if the blackbody temperature $T_{B}$ is known or estimated,

$$M_{\text{dust}} \propto \frac{f_{\nu}}{k_{\nu}B_{\nu}(T_{B})},$$

where $k_{\nu} \propto \nu^3$ is the mass absorption coefficient (e.g., Li & Draine 2001). Observers typically estimate galaxy dust masses using this technique and determine the dust temperature by fitting one (or perhaps two or three) blackbodies to a small number of far-infrared and submillimeter fluxes. However, this approach assumes that the large grains in all environments within a galaxy are heated to the same dust temperature and that they all exhibit the same dust emissivity properties.

Our "global" SED model allows a more realistic derivation of the dust mass, because it combines SEDs from the full range of heating environments. Moreover, since the large grains in the local SED models are in thermal equilibrium, equation (3) can appropriately be used to compute the local large-grain contribution. Then, equation (1) can be used to determine the actual global large-grain mass. The PAHs and very small grains together contribute, at most, an additional 14% to the total dust mass in our scheme (see § 5.4 in Dale et al. 2001).

The top panel of Figure 6 displays the ratio of the dust mass from the SED model to that predicted from a single modified blackbody approximation for the SED (again using eq. [3]). The blackbody temperature and dust emissivity are estimated from a fit to the simulated IRAS 100 $\mu$m, SIRTF 70 and 160 $\mu$m, and SCUBA 850 $\mu$m fluxes and displayed in the bottom panel. The dust mass is then estimated using the single-blackbody fit and the flux at each wavelength, as labeled in Figure 6. It is clear from the figure that using a single blackbody provides a significant underestimate of the dust mass, even for the most active galaxies for

### TABLE 1

| Wavelength (\(\mu m\)) | Before | After |
|-------------------------|--------|-------|
| SCUBA 850 ............. | 1.23 ± 0.07 | 0.39 ± 0.07 |
| ISOPHOT 170 .......... | 0.40 ± 0.09 | 0.20 ± 0.09 |
| ISOLWS 170 ........... | 0.51 ± 0.10 | 0.27 ± 0.11 |
| ISOLWS 158 .......... | 0.62 ± 0.08 | 0.43 ± 0.09 |
| ISOLWS 145 .......... | 0.59 ± 0.08 | 0.47 ± 0.08 |
| ISOLWS 122 .......... | 0.39 ± 0.06 | 0.37 ± 0.06 |
| ISOLWS 88 .......... | 0.38 ± 0.11 | 0.39 ± 0.11 |
| ISOLWS 63 .......... | 0.02 ± 0.11 | 0.02 ± 0.11 |
| ISOLWS 57 .......... | 0.09 ± 0.09 | 0.11 ± 0.09 |
| ISOLWS 52 .......... | -0.02 ± 0.12 | 0.03 ± 0.13 |

*Derived from a least-squares fit to log(flux observed/flux predicted by model) vs. log($f_{\nu}(60 \mu m)/f_{\nu}(100 \mu m)$), both “before” and “after” invoking the long-wavelength variable dust emissivity described by eq. (2).
which the undersampling factor is “only” a few. The reason for this large discrepancy lies in the single-blackbody approximation: the global SEDs are constructed from a combination of blackbody emission profiles that span a wide range of temperatures and emissivities; the various blackbody profiles significantly differ, especially in the far-infrared. Moreover, the very small grain emission, and to a lesser extent the emission from PAHs, affects the shape of the far-infrared SED at 70 \mu m (see Fig. 5 of Dale et al. 2001) and thus has an impact on the far-infrared flux densities.

The reason the ratios displayed in Figure 6 tend toward smaller values for the more active galaxies is easily explicable: for such galaxies, the effective spread in the radiation field intensity $U$ shrinks; the strong contributions from the hot, large grains in thermal equilibrium dominate the overall SED shape. However, it may seem a bit strange that the ratios in Figure 6 are a function of wavelength; why should the dust mass depend on wavelength? As alluded to above, the SED-based dust masses stem from a power-law combination of blackbodies over a large range of dust temperatures, whereas the blackbody-based dust masses are derived from a single fit to the broadband fluxes. The discrepancy between the single-blackbody fit and the model SED changes with wavelength, thus giving rise to the range of ratios in Figure 6.

5.3. The Infrared Energy Budget

Table 2 provides the infrared energy budget, updated from the version in Dale et al. (2001) to include the modifications to the far-infrared/submillimeter dust emissivity described in § 4.2. The table shows how much energy emerges in various infrared bands for model galaxies with different star formation activity, parameterized by the IRAS $f_{\nu}(60 \mu m)/f_{\nu}(100 \mu m)$ far-infrared color in column (1). The headings for columns (3)–(8) give the wavelength ranges over which the spectrum is integrated, and the table entries are the fraction of total infrared luminosity appearing in that range. The numbers are largely the same as those presented in Dale et al. (2001), except for the submillimeter range. After modifying the far-infrared/submillimeter dust emissivity, the 122–1100 \mu m flux fraction now spans 6%–32%, whereas the previous percentage range was 5%–39%. The models suggest that the far-infrared and submillimeter flux from even the coldest normal galaxies is no greater than one-third of the total infrared flux.

The spectral range in the column (7) corresponds to the FIR synthetic band (§ 5.1), a commonly quoted infrared flux quite often used as an indicator of the total level of star formation activity. This particular wavelength range accounts for about half of the total infrared emission for the majority
Sanders & Mirabel (1996) have also derived a relation for\( l_{100}\) explored further in\( x \) global star formation rate and the emission from the small-total infrared ratio, suggesting a tight link between the\( l_{2002} \) that the integrated 3–1000\( l_{m} \) infrared flux using a limited number of standard filters have wide applications. It is generally believed (e.g., Mann et al. 1996). Figure 7 gives the coefficients for all\( z \) out to 4. Equation (4) matches the model bolometric infrared luminosity, for all model SED shapes, to better than 1% at\( z = 0 \) and to within 4% for all redshifts smaller than 4 (see Fig. 7, bottom). For archival purposes, the analogous\( IRAS \)-based relation for normal galaxies is\( L_{\text{TIR}} = \zeta_{1} \nu L_{\nu}(25 \mu m) + \zeta_{2} \nu L_{\nu}(60 \mu m) + \zeta_{3} \nu L_{\nu}(160 \mu m) \),

\[
L_{\text{TIR}} = \zeta_{1} \nu L_{\nu}(25 \mu m) + \zeta_{2} \nu L_{\nu}(60 \mu m) + \zeta_{3} \nu L_{\nu}(160 \mu m) ,
\]

where \([\zeta_{1}, \zeta_{2}, \zeta_{3}] = [1.559, 0.7686, 1.347] \) for\( z = 0 \). The coefficients are derived from a singular value decomposition solution to an overdetermined set of linear equations (Press et al. 1996). Figure 7 gives the coefficients for all\( z \) out to 4. Equation (4) matches the model bolometric infrared luminosity, for all model SED shapes, to better than 1% at\( z = 0 \) and to within 4% for all redshifts smaller than 4 (see Fig. 7, bottom). For archival purposes, the analogous\( IRAS \)-based relation for normal galaxies is

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\]

where \([\zeta_{1}, \zeta_{2}, \zeta_{3}] = [2.403, -0.2454, 1.6381] \) for\( z = 0 \). At\( z = 0 \), the latter relation for\( IRAS \) fluxes reproduces the model bolometric infrared luminosities to better than 1% for most galaxies, although it does become inaccurate by about 7% for the colder galaxies; the\( IRAS \) 100\( \mu m \) band-pass does not extend to long enough wavelengths to effectively capture the coldest dust emission in nearby galaxies.

### 5.4. The Submillimeter-to-Radio Ratio

Efforts have been made to probe the utility of the submillimeter-to-radio flux ratio as a distance indicator (Lilly et al. 1999; Carilli & Yun 1999; Blain 1999; Dunne, Clements, & Eales 2000a; Barger, Cowie, & Richards 2000). The technique is influenced by the effect that star formation has on the emission in the far-infrared/submillimeter and in the radio: stars heat up dust grains that reprocess that energy as thermal emission, and stars that go supernova accelerate electrons throughout the interstellar medium, where they produce synchrotron emission (e.g., Helou & Bicay 1993). Since 850\( \mu m \) and 1.4 GHz lie on either side of the millimeter trough in normal galaxy (rest-frame) SEDs, and because the synchrotron emission increases with wavelength, whereas

|\( \log[f_{\nu}(60 \mu m)/f_{\nu}(100 \mu m)] \)| | \(3-5 \mu m\) | \(5-13 \mu m\) | \(13-20 \mu m\) | \(20-42 \mu m\) | \(42-122 \mu m\) | \(122-1100 \mu m\) |
|---|---|---|---|---|---|---|
| (1) | (2) | (3) | (4) | (5) | (6) | (7) |
| +0.10 | 1.09 | 0.5 | 3.4 | 4.8 | 32.8 | 52.4 | 6.1 |
| +0.00 | 1.41 | 0.8 | 4.8 | 4.4 | 28.0 | 53.3 | 8.7 |
| -0.10 | 1.64 | 1.3 | 6.7 | 4.0 | 22.7 | 52.7 | 12.5 |
| -0.20 | 1.82 | 1.7 | 8.9 | 3.8 | 17.8 | 50.8 | 16.9 |
| -0.30 | 2.00 | 2.2 | 11.2 | 3.7 | 13.6 | 47.9 | 21.5 |
| -0.50 | 2.56 | 3.0 | 15.3 | 3.8 | 7.4 | 38.3 | 32.2 |

\( a \) The quantity\( \alpha \) is the index of the power-law distribution described by eq. (1).
the submillimeter dust emission falls with wavelength, the ratio \( f_\nu(850 \mu m)/f_\nu(1.4 \text{ GHz}) \) increases with redshift. As one can infer from the spectra in Figure 5, the ratio is somewhat constrained for the suite of normal galaxies and should systematically grow larger for increasing redshifts (at least up to \( z \sim 5 \), before the far-infrared peak of the colder galaxies begins to enter the SCUBA 850 \( \mu m \) bandpass).

The envelope displayed in Figure 8 gives the predicted normal galaxy range of the submillimeter-to-radio flux density ratio as a function of redshift. Unless additional data on a given source can provide clues to its intrinsic infrared colors, the diversity of normal galaxy SEDs results in a rather broad envelope to the relation and thus limits its ultimate utility. For example, if \( \log(f_\nu(850 \mu m)/f_\nu(1.4 \text{ GHz})) \approx 1 \), then \( 0.2 \lesssim z \lesssim 1 \), and if \( \log(f_\nu(850 \mu m)/f_\nu(1.4 \text{ GHz})) \approx 2 \), then \( 1 \lesssim z \lesssim 2.8 \). Note that the envelope is defined by models based on nearby normal galaxies, whereas the submillimeter sources are likely different in at least some important aspects. For example, SMM J02399–0136 appears to be an extremely active hyperluminous infrared galaxy \( (L_{\text{FIR}} \sim 10^{13} L_\odot) \) with up to half of its luminosity deriving from an active galactic nucleus (AGN). Its SED may not be well represented in our models, since the most infrared luminous galaxies in the sample used for the models have \( L_{\text{FIR}} < 10^{12} L_\odot \) and no obvious AGN activity (Dale et al. 2000). This additional uncertainty as to the intrinsic SED of the high-redshift sources can only add to the difficulty of using this technique to constrain redshifts.

5.5. The Mid-Infrared–to–Submillimeter Ratio

An interesting and perhaps remarkable aspect of the plots displayed in Figure 5 is the approximately constant ratio between the mid-infrared and submillimeter fluxes; if far-infrared and submillimeter fluxes are normalized by the flux at 7 \( \mu m \), the ratios exhibit a narrow dispersion among normal galaxy model SEDs, generally in the 10%–20% range. Table 3 provides the ratios and their dispersions. The dispersion is more like 30%–50% for actual data. Combining the mid-infrared data from Dale et al. (2000) and the submillimeter from Dunne et al. (2000a) for 15 normal galaxies, \( \langle f_\nu(6.75 \mu m)/f_\nu(850 \mu m) \rangle \approx 1.5 \) (with a dispersion of \( \sigma \approx 0.8 \)). For comparison, Haas et al. (2001), who use a similar ratio\(^1\) as a probe of mid-infrared extinction, find \( \langle f_\nu(7.7 \mu m)/f_\nu(850 \mu m) \rangle \approx 4 \) (\( \sigma \approx 2 \)) for a sample of 20 normal galaxies. In a new study of five spatially resolved galaxies, Haas, Klaas, & Bianchi (2002) find a 30% dispersion within each galaxy: \( \langle f_\nu(6.75 \mu m)/f_\nu(850 \mu m) \rangle \approx 1.0 \) (\( \sigma \approx 0.3 \)).

An obvious application of this mid-infrared–to–submillimeter constancy would be the ability to estimate submillimeter fluxes using only mid-infrared data. Thus, if far-infrared data are also available, approximate dust masses are possible without even a measurement in the submillimeter. Such a tool would be particularly useful in quickly constraining the properties of galaxies in future large mid-infrared extragalactic surveys such as the SIRTF Wide-Area Infrared Extragalactic Survey (Lonsdale 2001), the Great Observatories Origins Deep Survey (Dickinson 2001), and the SIRTF First Look Survey (Shupe et al. 1999).

\(^1\) Haas et al. (2001) used the continuum-subtracted 7.7 \( \mu m \) peak flux. See also Klaas et al. (2001) and Haas et al. (2002).
Another application involves photometric redshifts. Beyond the local universe, the mid-infrared–to–submillimeter ratio should drop as the redshifted far-infrared peak approaches submillimeter wavelengths (see Fig. 5). Figure 9 displays two mid-infrared–to–submillimeter ratios as a function of redshift: $f_\nu(6.75\mu m)/f_\nu(850\mu m)$ and $f_\nu(15\mu m)/f_\nu(850\mu m)$. In contrast to the submillimeter-to-radio trends portrayed in Figure 8, the models predict the mid-infrared–to–submillimeter ratio to be fairly tight locally and to remain so at higher redshifts. Moreover, the rather steep profiles of the curves out to $z \sim 1\text{–}2$ let these ratios be better suited as distance indicators at intermediate redshifts. However, we caution that the suite of SED models is constructed to represent the average shapes of normal galaxies; the actual data can show large variations (e.g., see Fig. 10 of Dale et al. 2001). As noted above, the observed local dispersion is 2–3 times larger than what the models predict, so future high-redshift observations may show the actual normal galaxy envelopes to be larger by a similar factor than that indicated in Figure 9 (the data points in the figure may stem from extreme sources).

6. SUMMARY

The phenomenological model for the infrared spectral energy distributions for normal star-forming galaxies presented by Dale et al. (2001) does not adequately predict galaxy submillimeter fluxes and far-infrared fluxes beyond 100 $\mu m$. In this work, the empirical calibration is extended to submillimeter wavelengths; to better reproduce the far-infrared ISO and submillimeter SCUBA data, the model’s dust emissivity index is slightly changed as a function of the interstellar radiation field intensity. The modification is such that cold dust is removed from the previous modeling of the most quiescent regions and added to the most actively star-forming region models. Clearly, a power-law distribution of dust mass over different heating environments, coupled with a variable dust emissivity, is not the only possible approach to modeling galaxy infrared fluxes. Others have found that models involving only two thermal dust components and $\beta \sim 2$ can adequately represent galaxy far-infrared/submillimeter SEDs (e.g., Dunne & Eales 2001; Popescu et al. 2002), or perhaps a broken power law more accurately reflects the dust mass distribution. Nevertheless, several recent findings point to a dust emissivity that depends on environment and have led us to this approach.
Additional data from SIRTF, spanning a wide variety of
galaxy types and infrared wavelengths, should help to
improve upon these various approaches and point to the
most promising version.

The well-known far-infrared–to–radio correlation allows
us to extend the SEDs to even longer wavelengths and thus
to explore the feasibility of the submillimeter-to-radio ratio
as a redshift indicator. Although the range of spectral
shapes of normal galaxies unfortunately results in a rather
broad submillimeter-to-radio envelope, the relatively tight
mid-infrared–to–submillimeter ratio shows more promise
as a redshift tool. More data are needed, however, before
any real confidence can be placed in the latter’s redshift pre-

ciptability. Finally, we reach the important conclusion that
the standard method for estimating dust mass needs sub-
stantial revision, especially for the coldest galaxies, where
the underestimate is a factor of 10.

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