Utilizing Evidence Spans via Sequence-Level Contrastive Learning for Long-Context Question Answering

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Abstract

Long-range transformer models have achieved encouraging results on long-context question answering (QA) tasks. Such tasks often require reasoning over a long document, and they benefit from identifying a set of evidence spans (e.g., sentences) that provide supporting evidence for addressing the question. In this work, we propose a novel method for equipping long-range transformers with an additional sequence-level objective for better identification of supporting evidence spans. We achieve this by proposing an additional contrastive supervision signal in finetuning, where the model is encouraged to explicitly discriminate supporting evidence sentences from negative ones by maximizing the question-evidence similarity. The proposed additional loss exhibits consistent improvements on three different strong long-context transformer models, across two challenging question answering benchmarks – HotpotQA and QAsper.1

1 Introduction

Answering questions that require reasoning over a long sequence (e.g., multiple paragraphs or a long document consisting of multiple sections) is a challenging task (Dasigi et al., 2021; Pang et al., 2021). Research in this domain mostly concerns tasks that involve multiple passages (paragraphs or documents), including benchmarks like HotpotQA (Yang et al., 2018b) and QAsper (Dasigi et al., 2021). HotpotQA is a multi-hop QA benchmark over multiple paragraphs from Wikipedia and QAsper involves reading comprehension from long academic papers, where relevant information on a question could be spread across the paper, often resulting in complex entailment challenges.

Recent long-context transformers (Tay et al., 2021) have been successfully applied to long-context QA by processing and contextualizing information across the entire input. Prominent examples of long-context transformer models are Longformer (Beltagy et al., 2020) and BigBird (Zaheer et al., 2020) where instead of a full self-attention operation, they perform sparse self-attention over the input by using a local sliding window attention and a global attention mechanism to few specific input locations. To answer questions from long inputs that require multi-hop reasoning, it is often critical to identify a set of evidence spans (e.g., sentences or paragraphs) that provide relevant information for resolving the question. Prior work shows that jointly training long-context transformer models to perform evidence span extraction in addition to answer generation is important for achieving high performance (Beltagy et al., 2020; Dasigi et al., 2021). To jointly perform evidence extraction and question answering, these models utilize special sentence markers in the input; the final layer representation corresponding to these markers is then passed through a classification layer and is optimized using the cross-entropy loss in conjunction with the answer extraction/generation loss. We hypothesize that this cross-entropy loss does not explicitly capture relationships between the question and the candidate evidence spans. In this work, we propose a method for explicitly capturing question-evidence relationship with contrastive learning (see Fig. 1).

Driven by the intuition that better QA generalization requires finding supporting evidences for answering a question, we propose a supervised contrastive learning objective for long-context QA tasks at the finetuning stage. Contrastive learning has been recently applied to a variety of deep learning models in computer vision (Khosla et al., 2021; Chen et al., 2021; Chen et al., 2020; Chen and He, 2021) and NLP (Gao et al., 2021a; Gunel et al., 2021). Unlike

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Code is available at github.com/aviclu/seq-contrast-qa
the prior NLP related methods, we are the first to propose a novel model-agnostic contrastive loss for long-context transformers. Our proposed objective targets specifically the tokens that mark the question and evidence spans within input sequences, and unlike prior work, it is not based on individually encoding sentences or paragraphs. We show that our additional contrastive supervision provides consistent improvements on three different models and two long-context QA datasets, demonstrating its effectiveness and versatility.

2 Setup

Assume that we are given a question $q_i$ and a context $S_i = \langle s_1, ..., s_M \rangle$ consisting of $M$ sentences ($s_j$ can be also a document/paragraph/passage, depending on the dataset). From $C_i$, the task is to identify the correct answer $a_i$ and a set of $K$ evidence spans $S_i^+ = \{s_{i1}, ..., s_{iK} \}$ where $i_j$ are indices of the sentences that are the supporting evidence for answering the question $Q_i$.

As common in the input setup of long-context transformer models (Beltagy et al., 2020; Zaheer et al., 2020; Caciuaru et al., 2021), the question and context sentences are concatenated in a single long sequence with special tokens specifying sentence boundaries. Then the input is passed to the long-context transformer, and is trained to jointly identify the evidence sentences and extract/generate the answer. Concretely, for each example, we prepare the following concatenated input sequence:

$\text{Input}_i = [\langle s \rangle, Q_i, \langle / s \rangle, s_1, \langle / s \rangle, s_2, ..., \langle / s \rangle, s_M]$ where “,” is the string concatenation operation, $q_i$ and $s_j$ are sequences of tokens corresponding to the question and the $j$th sentence in the input context, and $\langle s \rangle$ and $\langle / s \rangle$ are special tokens representing the question and a context sentence, respectively (See Fig. 1 for an example). Then, a QA loss, which we denote by $L_{QA}$ is applied over the contextualized representation of each sentence token, and is optimized using supervision. $L_{QA}$ depends on the dataset and can take the form of a multi-task objective, representing multiple tasks in the context of QA (Dasigi et al., 2021) (e.g., evidence extraction, answer generation, etc.).

3 Sequence-level contrastive loss

To encourage the long-context transformer model to explicitly capture relationships between the question and evidence sentences, while performing the QA task, we introduce an additional sequence-level loss that compares and contrasts the question with context sentences. The additional proposed loss $L_C$ is based on the InfoNCE loss (Oord et al., 2018), and is applied over a triplet of vectors; it encourages the question and correct evidence representations to become closer to each other, while pushing the question and distracting target representations away. Formally, the contrastive loss is defined as the sum of negative log-likelihood losses over each example, where each loss term discriminates the positive units from negative ones, as follows:

$$L_{C_i} = - \log \sum_{x^+ \in S_i^+} \left( \frac{e^{\text{sim}(s^+, q_i)/\tau_k}}{\sum_{x \in S_i} e^{\text{sim}(s, q_i)/\tau_k}} \right),$$  

where $s^+$ is the positive supporting evidence marker token representation, $q_i$ is the vector representation corresponding to the question maker in the input ($\langle s \rangle$ in Fig. 1), $\tau_k$ is the configurable temperature hyperparameter, and $\text{sim}(\cdot)$ is a similarity metric, e.g., dot product ($\text{sim}(s, q) = s^\top q$) or cosine similarity ($\text{sim}(s, q) = \frac{s^\top q}{\|s\|\|q\|}$). Then the final aggregated loss is obtained by averaging over all the examples $L_C = \frac{1}{n} \sum_{i=1}^{n} L_{C_i}$.

We incorporate our additional contrastive loss into the main QA span extraction/generation loss.
\[ L = (1 - \lambda) \cdot L_{QA} + \lambda \cdot L_C, \]  
where \( \lambda \in [0, 1] \) is a hyper-parameter determining how much weight is assigned to each component of the total loss.

**Incorporating question types** Question types, if available in the dataset, can further guide our contrastive term and potentially improve the results by inserting more inductive bias to the model. Following Iter et al. (2020), we can also define the similarity function as the bilinear distance according to different question types (e.g., yes/no, generative, non-answerable, etc).

\[ \sim_k(s, q) = s^T W_k q, \]  
where \( k \) is the expected question type (which is given as a label in the training set), and \( W_k \) is the corresponding allocated learnable matrix. For example, in the HotpotQA dataset, we are given three question types: \( k \in \{\text{yes, no, span}\} \). Such learnable linear projections ensure that a specific subspace per question type exists. We additionally incorporate different temperature hyperparameters \( \tau_k \) based on each question type in Equation 1 (see the ablation Table 3 for the effect of using different temperature per question type). The model then can leverage this information as solving QA tasks might require knowledge about question-type relations.

The dimensions of the proposed \( W_k \) tend to be large (because of the dimensions of the transformer’s hidden-layers).\(^2\) Hence, following Barkan et al. (2020), we introduce new non-square linear projections instead of using \( W_k \):

\[ \sim_k(s, q) = \frac{s_k^T q_k}{\|s_k\| \|q_k\|}, \]  
where we set \( s_k = W_k^S s, q_k = W_k^Q q \), and \( W_k^S \) (or \( W_k^Q \)) is the learnable matrix that projects \( s \) (or \( q \)) into a lower dimension, in the \( k \)th question-type sub-space. Note that a correct answer projected into a lower dimension, in the sub-space of the wrong question type is considered as wrong. We can further integrate this into the denominator of the term inside \( L_C \), namely, the representations of \( s \) and \( q \) under the incorrect question types.

While contrastive learning has recently emerged as a useful tool for improving NLP tasks, in both finetuning and pretraining phases (Gunel et al., 2021), prior work applied this technique primarily for *inter-sequence* representation enhancement, e.g., better sentence representations in a Siamese setup (Iter et al., 2020; Luo et al., 2020; Gao et al., 2021a), whereas we apply this learning method in an *intra-sequence* manner, aiming at improving mutual contextual representations, considering the same sequence.

### 4 Experimental Setup and Results

In this section, we provide details about the experiments that we conducted and their outcomes.

#### 4.1 Experimental Setup

As previously stated, we conjecture that our additional contrastive loss term can be useful for learning meaningful representations for modeling long-range relationships, which are typically required solving tasks that involve long-document or multi-document processing.

Accordingly, in order to demonstrate the advantage of our method, we performed an extensive evaluation using the recent QA\textsuperscript{per} dataset (Dasigi et al., 2021) and the well-known HotpotQA dataset (Yang et al., 2018a), which share the input form (see Section 2).

**QA\textsuperscript{per}** (Dasigi et al., 2021) is a long-document QA dataset which was built over academic papers, where NLP practitioners were recruited to generate questions following the title and the abstract of a particular paper, as well as creating the correct evidence and answers to those questions out of the entire paper. More than half of the examples in QA\textsuperscript{per} require collecting evidences from multiple paragraphs in the given paper. For this benchmark, \( L_{QA} \) represents the sum of the teacher-forced text generation and paragraph classification loss functions, in a multi-task training setup.

We replicated the experiments described in Dasigi et al. (2021); we finetuned the LED-base model,\(^3\) and evaluated it on the question answering and evidence selection tasks. For further details about the structure of the dataset and finetuning, see Appendix A.1.

**HotpotQA** (Yang et al., 2018a) introduced the task of multihop question answering (in the reading comprehension setting), where the inputs are

\(^2\) We end up with \( W_k \in \mathbb{R}^{768 \times 768} \) for base-sized models and \( W_k \in \mathbb{R}^{1024 \times 1024} \) for large-sized models.

\(^3\) According to Dasigi et al. (2021), LED-base outperforms LED-large over QA\textsuperscript{per}. 
Table 1: Performance change when applying our additional loss $L_T$ to the LED SOTA model on QAsper (the metric is Answer-$F_1$).

| Input          | Extractive Dev. | Extractive Test | Abstractive Dev. | Abstractive Test | Yes/No Dev. | Yes/No Test | Unanswerable Dev. | Unanswerable Test | Evidence Dev. | Evidence Test | Overall Dev. | Overall Test |
|----------------|-----------------|-----------------|------------------|------------------|-------------|-------------|-------------------|-------------------|----------------|---------------|--------------|--------------|
| LED (2020)     | 26.1            | 31.0            | 16.6             | 15.8             | 67.5        | 70.3        | 28.6              | 26.2              | 23.9          | 29.9          | 29.1         | 32.8         |
| $+L_T$ (Δ)     | +0.2            | +0.2            | +0.8             | +1.0             | +1.6        | +0.2        | +1.5              | +1.9              | +1.0          | +0.7          | +0.9         | +0.7         |

Table 2: HotpotQA-distractor results ($F_1$) for the dev set. We use the “base” and “large” model size results of CDLM and the Longformer for direct comparison. Ans: answer span, Sup: Supporting facts.

| Model            | Ans  | Sup | Joint |
|------------------|------|-----|-------|
| Longformer-base (2020) | 74.5 | 83.9 | 64.5  |
| $+L_T$ (Δ)       | 74.7 | 86.3 | 66.3  |
| CDLM-base (2021) | 81.3 | 88.3 | 73.2  |
| $+L_T$ (Δ)       | 81.3 | 89.1 | 73.8  |

Table 3: Similarity function ablation results (Joint $F_1$) of CDLM and our loss term on the HotpotQA-distractor dev set.

| Model               | Joint | Δ    |
|---------------------|-------|------|
| CDLM-large + $L_T$ (Eq 4) | 74.6  | 0.4  |
| **sim(·)** is the dot product | 74.7  | 0.4  |
| **sim(·)** is the cosine similarity | 74.0  | 0.6  |
| **sim(·)** is the bilinear distance (Eq 3) | 73.7  | 0.9  |

4CDLM was shown to be an effective long-range encoder model for HotpotQA. 5we used the code from https://github.com/aviclu/CDLM/tree/main/pretraining of the Longformer and CDLM. For further details about the structure of the dataset and finetuning, see Appendix A.2.

For both QAsper and HotpoQA, we performed a similar grid search for determining the hyper-parameters of the contrastive loss (see more details in Appendix B).

4.2 Results

Main results We adopted the same evaluation metrics of original works, from Dasigi et al. (2021) and Beltagy et al. (2020) (where the reader is referred for more details). Tables 1 and 2 illustrate the evaluation results over the QAsper and HotpoQA datasets, respectively. We show the performance difference of adding our additional loss term with “$+L_C$”. The addition of our contrastive loss term exhibits the best performance among all the models and benchmarks, clearly demonstrating its consistent advantage. Note that maximizing the question-evidence similarity resulted also in the evidence detection improvement – see the “Evidence” and the “Sup” metrics in Table 1 and in Table 2, respectively.

Ablations Table 3 demonstrates the ablation study results for evaluating the effectiveness of our design decisions. Using a constant temperature parameter for all question types, as well as using a different, degenerated similarity functions exhibits a lower performance results. Notably, by the last row in Table 3 we see that treating correct answers that are projected to the wrong question type as negatives seems to slightly improve the results. Overall, the ablation study shows the advantage of using Eq. 4 as a similarity function that provides an fine-grained, expressive modeling for question types, since it handles each question type in its own subspace. An additional theoretical justification to our contrastive learning is provided in (Gao et al., 2021b), where we can imply that our loss term improves the uniformity and therefore the expressiveness of the question and evidence representations.
Figure 2: PCA plots of the learned question and answer token embeddings on the HotpotQA validation set, comparing early training epochs results (left) and results after model convergence (right). The wrong evidence representations correspond to both wrong evidences, or correct evidences using the wrong question type projections (our soft negatives).

Analysis We apply PCA over the relevant normalized token representations of the validation data of HotpotQA (i.e., the question and answers representations in Fig. 1), and depicted them in 2. The projected representations of the correct and wrong answers are equally distributed at the beginning of the training (left figure). After several epochs when the model converged (right figure), the answer representations’ manifold got closer to the questions’ representations (in terms of radial distance). Each beam in the figure corresponds to a different question type (there are 3 in HotpotQA). The correct evidence representations (green dots) are the closest among the whole answer representations, confirming that our additional contrastive loss term generalizes and maximizes the question-evidence similarity.

5 Conclusion

In this work, we propose an effective sequence-level contrastive loss for improving the performance of long-range transformers in solving QA tasks that require reasoning over long contexts. We demonstrate consistent improvement when using our approach on three different models over two different benchmarks. In future work, we would like to explore variations of our proposed supervised loss on other long-context tasks, such as long document summarization.

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### A Datasets and Finetuning Details

In this section, we provide details, regarding fine-tuning and hyper-parameter configuration, over the benchmarks we used during our experiments.

#### A.1 QAsper

Since some of the questions included in QAsper are not answerable, we apply our contrastive loss only over examples that are answerable and contain at least one evidence sentence.

We train all models using the Adam optimizer (Kingma and Ba, 2014) and a triangular learning rate scheduler (Howard and Ruder, 2018) with 10% warmup. To determine number of epochs, peak learning rate, and batch size, we performed manual hyperparameter search on a subset of the training data. We searched over \{1, 3, 5\} epochs with learning rates \{(1e^{-3}, 3e^{-3}, 5e^{-5}, 9e^{-5})\}, and found that smaller batch sizes generally work better than larger ones. Our final configuration was 10 epochs, peak learning rate of 5e^{-5}, and batch size of 2, which we used for all reported experimental settings. When handling full text, we use gradient checkpointing (Chen et al., 2016) to reduce memory consumption. We run our experiments on a single RTX 8000 GPU, and each experiment takes 30–60 minutes per epoch.

#### A.2 HotpotQA

We used the HotpotQA-distractor dataset (Yang et al., 2018a). Each example in the dataset includes a question and 10 paragraphs from different documents, extracted from Wikipedia. Two gold paragraphs include the relevant information for properly answering the question, mixed and shuffled with eight distractor paragraphs (for the full dataset statistics, see Yang et al. (2018a)). There are two goals for this task: detecting the supporting facts, i.e., evidence sentences, as well as extraction of the correct answer span.

For preparing the data for training and evaluation, we follow the same finetuning scheme of the CDLM (Caciularu et al., 2021) and the Longformer (Beltagy et al., 2020); For each example, we concatenate the question
and all the 10 paragraphs in one long context. We particularly use the following input format with special tokens and our document separators: “[CLS] [q] question [/q] ⟨doc-s⟩⟨t⟩ title1 ⟨/t⟩ ⟨s⟩ sent1,1 ⟨/s⟩ ⟨s⟩ sent1,2 ⟨/s⟩ ⟨doc-s⟩ ... ⟨t⟩ ⟨doc-s⟩ title2 ⟨/t⟩ ⟨s⟩ sent2,1 ⟨/s⟩ ⟨s⟩ sent2,2 ⟨/s⟩ ⟨doc-s⟩ ...” where [q], [/q], ⟨t⟩, ⟨/t⟩, ⟨s⟩, ⟨/s⟩, [p] are special tokens representing, question start and end, paragraph title start and end, and sentence start and end, respectively. The new special tokens were added to the models vocabulary and randomly initialized before task finetuning. We use global attention to question tokens, paragraph title start tokens as well as sentence tokens. The model’s structure is taken from Beltagy et al. (2020).

As in Beltagy et al. (2020); Caciularu et al. (2021), we finetune our models for 5 epochs, using a batch size of 32, learning rate of 1e-4, 100 warmup steps. Finetuning on our models took ~6 hours per epoch, using four 48GB RTX8000 GPUs for finetuning our models.

B Contrastive Loss Details

In this section, we provide the details for reproducing our contrastive term, which is relevant for both QAsper and HotpotQA.

We searched over $d \times \{d, \frac{d}{2}, \frac{d}{4}, \frac{d}{8}\}$ to determine the linear projections’ dimensions, where $d$ is the model’s hidden layer representation dimension (it depends on the size of the model).

In order to determine the temperature hyperparameter $\tau$, we searched over $\{0.2, 0.4, 0.6, 0.8, 1.0\}$ per question type (if applicable).

We also applied dropout, with a rate of $p = 0.1$, over the linear projections, which consistently improved the results over all the benchmarks.