Ferromagnetic in-plane spin fluctuations in Na$_x$CoO$_2$ observed by neutron inelastic scattering

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We present neutron scattering spectra taken from a single crystal of Na$_{0.75}$CoO$_2$, the precursor to a novel cobalt-oxide superconductor. The data contain a prominent inelastic signal at low energies ($\sim 10$ meV), which is localized in wavevector about the origin of two-dimensional reciprocal space. The signal is highly dispersive, and decreases in intensity with increasing temperature. We interpret these observations as direct evidence for the existence of ferromagnetic spin fluctuations within the cobalt-oxygen layers.

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Sodium cobalt oxide (Na$_x$CoO$_2$) has become of considerable interest in the past few years owing firstly to the report of a large thermoelectric power coupled with low resistivity in single crystals of Na$_{0.5}$CoO$_2$ [1], and second, to the serendipitous discovery of superconductivity at temperatures below $T_c \simeq 5$ K in Na$_{x}$CoO$_2\cdot y$H$_2$O ($x \simeq 0.3, y \simeq 1.3$) formed by hydration of precursor Na$_x$CoO$_2$ [2]. The enhanced thermoelectric properties of Na$_x$CoO$_2$ make it potentially important for thermoelectric applications, and the existence of superconductivity in the hydrated compound raises very interesting questions about the pairing mechanism in relation to the cuprate and ruthenate superconductors.

Like the superconducting cuprates and ruthenates, the structure of Na$_x$CoO$_2$ is layered, consisting in this case of triangular CoO$_2$ sheets separated by layers of Na$^+$ ions. Incorporation of water increases the sheet separation and decreases the Na content. Metallic behaviour is achieved by doping the Mott-insulating CoO$_2$ sheets with electrons donated by Na, which create Co$^{3+}$ ions with zero spin in a background of Co$^{4+}$ carrying spin $S = \frac{1}{2}$. The enhanced thermopower has been ascribed to a large spin entropy arising from strong electron-electron interactions in the CoO$_2$ sheets [3].

Superconductivity in the hydrated compound is observed in a narrow range of composition centred around $x = 0.3$ [4]. Although the pairing mechanism has not yet been established, a number of experimental studies have uncovered evidence suggesting that the superconductivity in this material is unconventional [5]. Several attempts [6, 14, 15, 16] to understand the superconductivity have been based on Anderson’s resonating valence bond (RVB) idea [11], which describes a singlet quantum spin liquid ground state stabilized by frustration. The $S = \frac{1}{2}$ triangular lattice could in principle support an RVB state providing the coupling between nearest-neighbour spins were antiferromagnetic, as suggested by the high temperature susceptibility of both superconducting Na$_{0.5}$CoO$_2\cdot 1.3$H$_2$O [12] and precursor Na$_x$CoO$_2$ [13]. Among alternative scenarios, the possibility of spin-triplet superconductivity has been analyzed by several authors [4, 14, 15, 16], and has received support from resonance experiments [5]. The existence of ferromagnetic correlations, which would open the door to $p$-wave spin-triplet pairing, was predicted from density-functional calculations for Na$_x$CoO$_2$ with $x = 0.3-0.7$ [17, 18]. The predicted ferromagnetic instability was found to be robust to the structural changes associated with hydration [18]. Proximity to a ferromagnetic instability is suggested by an irreversible magnetic transition at $T_m = 22$ K in Na$_{x}$CoO$_2$ [19], an upturn in the low temperature susceptibility of Na$_x$CoO$_2$ [19, 20] and Na$_{0.35}$CoO$_2\cdot 1.3$H$_2$O [12], and has also been inferred from some nuclear relaxation measurements [5].

The importance of spin degrees of freedom, both to explain the thermopower and in most of the theories of superconductivity proposed so far, makes it essential to have experimental information on magnetic correlations, especially to establish whether the dominant in-plane coupling is ferromagnetic or antiferromagnetic. This information can most directly be obtained from neutron scattering measurements on single crystal samples. Crystals of superconducting compositions large enough for neutron scattering are not yet available. Here we present the first neutron inelastic scattering spectra of the precursor compound Na$_x$CoO$_2$. The data provide strong evidence for the existence of ferromagnetic spin correlations within the CoO$_2$ layers.

Single crystals of Na$_{0.75}$CoO$_2$ were grown by the floating-zone method in an image furnace [21]. A crystal of size $\sim 10 \times 8 \times 3$ mm$^3$ was cleaved from the zone-melted rod. Magnetization and powder X-ray diffraction measurements made on samples taken from adjacent parts of the same crystal rod showed no impurity phases within the detectable limit of $\sim 2\%$.

Neutron inelastic scattering measurements were made on the MAPS spectrometer at the ISIS Facility. MAPS is a time-of-flight instrument equipped with a large pixel-
lated detector surrounding the incident beam direction. Neutrons of well-defined incident energy are delivered to the sample in short pulses. Spectra in each pixel are recorded as a function of neutron time-of-flight, and subsequently transformed into an intensity array in \((\mathbf{Q}, E)\) space, where \(\mathbf{Q} = \mathbf{k}_i - \mathbf{k}_f\) is the scattering vector (the difference between the incident and final neutron wavevectors) and \(E\) is the energy transferred to the sample. The intensity was converted into an absolute cross section by the factor \(k_i/k_f\) \([21]\), where \(E_f\) is the final energy.

The crystal was attached to a copper rod and mounted on a closed-cycle cooler. Measurements were made at several temperatures between 6 K and room temperature. Typical counting times were 36 hours at an average proton current of 170 \(\mu\)A. An initial examination by neutron Laue diffraction showed that the crystal contained several grains with an overall mosaic spread of \(\sim 10\) degrees. To maintain good \(\mathbf{Q}\) resolution we employed relatively low incident energies \((E_i = 40\) meV and 60 meV\), and restricted our measurements to small scattering angles.

The physical properties of Na\(_{x}\)CoO\(_2\) are highly two-dimensional (2D) \([1]\). It is likely, therefore, that any magnetic correlations between the CoO layers are very weak, and hence that the magnetic scattering is independent of the component of \(\mathbf{Q}\) parallel to the crystal \(c\) axis. For an initial survey, therefore, we aligned the crystal with the \(c\) axis parallel to the incident neutron beam, so that the area detector recorded the energy spectrum over a large region of 2D reciprocal space (\(\geq 1\) Brillouin zone) spanned by the \(\mathbf{a}^*\) and \(\mathbf{b}^*\) reciprocal lattice basis vectors of the triangular lattice in the CoO\(_2\) plane \([22]\). The energy range probed in this configuration was from 2 meV to 50 meV. By taking a series of constant-energy slices we made a search of \((\mathbf{Q}_{2D}, E)\) space, where \(\mathbf{Q}_{2D} = h\mathbf{a}^* + k\mathbf{b}^* \equiv (h, k)\) is the in-plane component of the scattering vector. The only signal we found that was clearly in excess of the background in this energy range was distributed symmetrically around the unscattered beam, i.e. \(\mathbf{Q}_{2D} = (0, 0)\). In particular, there was no observable signal at wavevectors corresponding to antiferromagnetic correlations between adjacent Co sites.

To investigate the observed signal further we rotated the crystal by 30 degrees, so that more of the \(\mathbf{Q}_{2D} = (0, 0)\) scattering would be recorded in the detectors adjacent to the unscattered beam. Figure 1 displays the neutron intensity averaged over the energy range 8–12 meV and projected onto the \(a^*b^*\) plane. The unscattered beam passes through the centre of the blank rectangle where there are no detectors. The map shows an enhanced signal roughly twice the background in the detectors to the right of the blank rectangle. This is the same signal observed in the unrotated orientation, but now it has shifted to the right due to the rotation of the crystal. This confirms that the signal is centred on \(\mathbf{Q}_{2D} = (0, 0)\), part of the signal being missing where it overlaps the blank rectangle. Away from this feature the intensity landscape is featureless. We remark here that the peak is much broader in wavevector than the resolution. The latter is dominated by the crystal mosaic, which causes a spread in wavevector of \(\sim 0.05a^*\) at this energy, whereas the peak has a width of \(\sim 0.2a^*\).

Figure 2 shows the energy dependence of the scattering measured at a temperature of 6 K. To construct this scan we averaged the data over a rectangular box (marked A in Fig. 1) centred on \((0, 0)\) enclosing the peak. Two distinct features stand out above the background: (1) a peak centred near 20 meV, and (2) an increase in scattering with decreasing energy below 15 meV. The signal appears to level off below 10 meV, but this trend cannot be established definitively from the current data because at low energies a significant proportion of the signal is...
implies that the correlations are ferromagnetic within the
fact that the scattering is localized about
magnetic correlations decrease with temperature. The
low energy feature suggests a magnetic origin because
20 meV peak is an optic phonon.
200 K in Na
This is consistent with the data in Fig. 3(b). As there is currently no
evidence for magnetic order at temperatures as high as

The temperature dependence is shown at average ener-
gies of 10 meV and 20 meV, respectively. The peak in the
10 meV cut is seen to decrease with temperature, and at
200 K is almost indistinguishable from the background.
By contrast, the 20 meV peak increases with tempera-
ture.
The increase in intensity with temperature of the
20 meV peak suggests that this scattering arises from
a bosonic excitation, such as a phonon. The scattering
intensity is then expected to vary in proportion to
the factor \( \{1 - \exp(-\hbar\omega/k_B T)\}\)\(^{-1} \) \([21]\), which increases by \(~ 50\% \) from 6 K to 200 K. This increase is consist-
tent with the data in Fig. 3(b). As there is currently no
evidence for magnetic order at temperatures as high as
200 K in Na\(_{0.75}\)CoO\(_2\) \([19]\), the most likely origin of the
20 meV peak is an optic phonon.
On the other hand, the temperature dependence of the
low energy feature suggests a magnetic origin because
magnetic correlations decrease with temperature. The
fact that the scattering is localized about \(Q_{2D} = (0,0)\)
implies that the correlations are ferromagnetic within the
ab plane.

Having concluded that the low energy signal at \(Q_{2D} =
(0,0)\) corresponds to 2D ferromagnetic correlations we
now turn to its energy spectrum. Fig. 4 displays a set of
constant-energy cuts along the line marked X in Fig. 4 through the data collected at \(T = 6\) K. The 6.5 meV cut shows a single peak centred at \((0,0)\), but with increasing energy the peak broadens and decreases in amplitude. In addition, the lineshapes in the 10 meV and 14 meV cuts are distinctly flat-topped, suggestive of two almost-
resolved peaks either side of \(\zeta = 0\). Although the extent of our data is limited, it is clear that the magnetic scattering is highly dispersive and that it extends above 16 meV into the energy range where the optic phonon dominates the signal.
Finally, we consider the energy-integrated cross sec-
tion, and compare it with the local-moment sum rule. In-
tegrating the magnetic signal between 5 meV and 16 meV
and averaging the result over one 2D Brillouin zone we
obtain \(~ 1\text{mb sr}^{-1}\text{f.u.}^{-1}\). Neglecting the magnetic
form factor, the energy-integrated, \(Q\)-averaged scatter-
ing from a system of local moments with spin \(S\) is
\(\Sigma = \frac{1}{8}(\gamma q_0)^2 g^2 S(S + 1)\) per spin, where \(\gamma = 1.913\),
\(q_0 = 2.818 \times 10^{-15}\) m, and \(g\) is the Landé factor \([21]\).
Taking as a reference the values \(S = \frac{1}{2}\) and \(g = 2\), we find
\(\Sigma = 145\text{mb sr}^{-1}\text{spin}^{-1}\). In Na\(_{0.75}\)CoO\(_2\) only a quarter of
the Co ions carry a spin, on average, so this would reduce
the expected cross section to \(~ 36\text{mb sr}^{-1}\text{f.u.}^{-1}\). This
is much larger than the inelastic scattering cross section
we have observed, which suggests that there is consid-
erable spectral weight outside the energy range probed
in our experiment. Some of this will undoubtedly be at
higher energies, since the measured spectrum appears to extend above 16 meV, but we would also expect some of the weight to be below 2 meV in the form of elastic or quasielastic scattering. In particular, although we collected elastic scattering data over a wide range of reciprocal space we did not probe along the (0,0,1) line, so any Bragg peaks associated with in-plane ferromagnetic order could not have been measured. Full 3D ferromagnetic order is excluded by the magnetization data [16], but a spin arrangement with in-plane ferromagnetic order and a spin-density wave modulation perpendicular to the planes, e.g. an antiferromagnetic stacking along the c axis, would be compatible with our results.

The measurements reported here show conclusively that there exist strong ferromagnetic in-plane correlations in Na$_{0.75}$CoO$_2$, with an energy scale much larger than that set by the observed magnetic ordering temperature ($T_m = 22$ K [17]). Interestingly, the excitation spectrum resembles that found in nearly-ferromagnetic metals, such as Ni$_3$Ga [23] and Pd [24], characterized by strongly damped or overdamped ferromagnons [25]. This finding is in remarkable accord with the picture described by Singh based on density-functional calculations in the local-density approximation (LDA) [17,18]. He predicts a weak itinerant ferromagnetic ground state for all doping levels in the range $x = 0.3 - 0.7$, and suggests that quantum spin fluctuations would in practice suppress the tendency for ordering. The spin excitation spectrum would then resemble that of overdamped ferromagnons, consistent with what is observed here.

There is good reason to believe that the ferromagnetic correlations found in Na$_x$CoO$_2$ will also be present in the superconducting compound, and may therefore play a role in the mechanism of superconductivity. The LDA calculations, which successfully described the present results, also predict a ferromagnetic ground state with the strained cell and Na doping of the hydrated superconductor [18]. This, together with the evidence reported for unconventional superconductivity [3], raises the possibility of $p$-wave spin-triplet pairing, a state thought to occur in Sr$_2$RuO$_4$ [26]. Unlike the ruthenate, however, the superconductivity in hydrated Na$_x$CoO$_2$ has not been reported sensitive to impurities, and the most prominent spin fluctuations in Sr$_2$RuO$_4$ are not ferromagnetic but instead have an incommensurate wavevector [27]. Nevertheless, the proximity to a ferromagnetic phase in each case suggests the mechanism of superconductivity in the two materials may share some common features.

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