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Optimization of graph construction can significantly increase the power of structural brain network studies

Eirini Messaritaki\textsuperscript{a,b,c,*}, Stavros I. Dimitriadis\textsuperscript{a,c,d,e,f}, Derek K. Jones\textsuperscript{a,d,e}

\textsuperscript{a} Cardiff University Brain Research Imaging Centre (CUBRIC), School of Psychology, Cardiff University, Maindy Road, Cardiff, CF24 4HQ, UK
\textsuperscript{b} BRAIN Biomedical Research Unit, Cardiff University, Maindy Road, Cardiff, CF24 4HQ, UK
\textsuperscript{c} Division of Psychological Medicine and Clinical Neurosciences, School of Medicine, Cardiff University, Cardiff, CF24 4HQ, UK
\textsuperscript{d} School of Psychology, Cardiff University, 70 Park Place, Cardiff, CF10 3AT, UK
\textsuperscript{e} Mary McKillop Institute for Health Research, Faculty of Health Sciences, Australian Catholic University, Melbourne, Australia
\textsuperscript{f} Neurinformatics Group, Cardiff University Brain Research Imaging Centre, School of Psychology, Cardiff University, Cardiff, United Kingdom

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Structural brain networks derived from diffusion magnetic resonance imaging data have been used extensively to describe the human brain, and graph theory has allowed quantification of their network properties. Schemes used to construct the graphs that represent the structural brain networks differ in the metrics they use as edge weights and the algorithms they use to define the network topologies. In this work, twenty graph construction schemes were considered. The schemes use the number of streamlines, the fractional anisotropy, the mean diffusivity or other attributes of the tracts to define the edge weights, and either an absolute threshold or a data-driven algorithm to define the graph topology. The test-retest data of the Human Connectome Project were used to compare the reproducibility of the graphs and their various attributes (edges, topologies, graph theoretical metrics) derived through those schemes, for diffusion images acquired with three different diffusion weightings. The impact of the scheme on the statistical power of the study and on the number of participants required to detect a difference between populations or an effect of an intervention was also calculated.

The reproducibility of the graphs and their attributes depended heavily on the graph construction scheme. Graph reproducibility was higher for schemes that used thresholding to define the graph topology, while data-driven schemes performed better at topology reproducibility (mean similarities of 0.962 and 0.984 respectively, for graphs derived from diffusion images with $b = 2000 \text{ s/mm}^2$). Additionally, schemes that used thresholding resulted in better reproducibility for local graph theoretical metrics (intra-class correlation coefficients (ICC) of the order of 0.8), compared to data-driven schemes. Thresholded and data-driven schemes resulted in high (0.86 or higher) ICCs only for schemes that use exclusively the number of streamlines to construct the graphs. Crucially, the number of participants required to detect a difference between populations or an effect of an intervention could change by a factor of two or more depending on the scheme used, affecting the power of studies to reveal the effects of interest.

\textbf{1. Introduction}

The view that the human brain is a network of cortical and subcortical areas connected via white matter tracts emerged several decades ago and has been very useful in characterizing brain structure and function in both healthy participants and diseased populations (Hagmann et al., 2008; Griffa et al. (2013); Caeyenberghs and Leemans (2014); Fischer et al. (2014); van den Heuvel and Fornito (2014); Yuan et al. (2014); Baker et al. (2015); Collin et al. (2016); Drakesmith et al. (2015); Aerts et al. (2016); Nelson et al. (2017); Vidauerre et al. (2018); Imms et al.

\textbf{Abbreviations:} CM, connectivity matrix; FA, fractional anisotropy; GLM, general linear model; ICC, intra-class correlation coefficient; MD, mean diffusivity; NS, number of streamlines; OMST, orthogonal minimal spanning tree; PS, percentage of streamlines; RD, radial diffusivity; SD, standard deviation; SLD, streamline density; TL, tract length; TV, tract volume; WM, white matter.

\textit{E-mail address:} messaritakie2@cardiff.ac.uk (E. Messaritaki).

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(2019), to name just a few of the studies). Structural networks can be constructed using data collected non-invasively via magnetic resonance imaging (MRI) and diffusion MRI (dMRI). Graph theory allows quantification of the organizational properties of structural brain networks by using graphs to represent those networks (Bullmore and Sporns 2009) and references therein).

For inferences drawn from graph theoretical analyses of structural brain networks to be reliable, it is essential that the graphs representing the structural networks reflect the true structural organization of the brain. If that is the case, such graphs are bound to be reproducible, within experimental error, when generated from data collected at different times, in the absence of any true changes in the structural connectome. Conversely, this means that graphs that are not reproducible in the absence of age-related changes or intervention-induced plasticity are not reliable in representing the structural organization of the human brain. This is important because various graph construction schemes have been presented in the literature that use different techniques to perform tractography, define graph topology and assign edge-weights, all producing graphs that are quite different from each other, with different levels of robustness and reproducibility. Using schemes that result in highly reproducible graphs and graph-attributes means that any observed changes (in longitudinal studies) or differences between populations (in comparative studies) can be reliably attributed to maturation or to differences between populations respectively, rather than to random fluctuations resulting from experimental or analysis errors. Additionally, high reproducibility and low within-participant variability results in higher power for the studies and therefore a lower number of required participants, which in turn results in reduction of the cost and resources required for the study. Several papers have investigated different aspects of the reproducibility of structural brain networks and their graph theoretical metrics (Dennis et al., 2012; Owen et al., 2013; Buchanan et al., 2014; Smith et al., 2015; Owen et al., 2013, 2015; Dimitriadis et al., 2015, 2017b; Yuan et al., 2018), each using a specific scheme for constructing the graphs, predominantly using data acquired with low diffusion weightings ($b$-values of up to $1500$ s/mm$^2$). The work of Roine et al. (2018) also investigated a higher diffusion weighting of $b = 3000$ s/mm$^2$.

In this work, we compared the reproducibility of structural brain networks generated with different graph-construction schemes for three different diffusion weightings. We investigated the reproducibility of the graphs themselves as well as their topologies, edge-weights and graph theoretical metrics. The article is organized as follows: Section 2 details the data, the software and algorithms used to perform the tractography, construct the graphs representing the structural networks, and perform the comparative analyses. Section 3 contains a comparison of the graphs derived using different graph-construction schemes and describes the results for the reproducibility of the graphs and their various attributes. Finally, it presents sample calculations for the number of participants required for different studies, for the different graph-construction schemes. Section 4 includes a discussion of the significance of our results and the ways they can impact graph theoretical studies of structural brain networks in the future. We conclude with Section 5. To the best of our knowledge, this is the first time that graph-construction schemes for structural brain networks have been compared in terms of their reproducibility across a wide range of diffusion weightings, in particular with an aim to inform decisions on the number of participants required in related studies.

### 2. Methods

All analyses were performed using MATLAB (MATLAB and Statistics Toolbox Release, 2015a; The MathWorks, Inc., Massachusetts, United States), unless otherwise stated.

#### 2.1. Data

We used the Human Connectome Project (HCP) (Van Essen et al., 2013; Sotiropoulos et al., 2013b; Glasser et al., 2013) test-retest MRI and diffusion-MRI data, in which participants were scanned twice. The time interval between the two scans of each participant ranged between 1.5 and 11 months, and the age range of the participants was 22–41 years. This scan-rescan time interval is shorter than that expected for measurable maturation-induced structural changes to occur.

The diffusion-weighted images (DWIs) have resolution of $(1.25 \times 1.25 \times 1.25)$ mm$^3$, and were acquired for three different diffusion weightings ($b$-values: $1000$ s/mm$^2$, $2000$ s/mm$^2$ and $3000$ s/mm$^2$). We used the data from 37 participants for whom there were 90 gradient directions for each $b$-value. The HCP acquisition details are described in Sotiropoulos et al. (2013b); Feinberg et al. (2010); Moeller et al. (2010); Setsompop et al. (2012); Sotiropoulos et al. (2013a); Xu et al. (2012). We performed the analyses described below separately for the DWIs collected with each diffusion weighting.

#### 2.2. Tractography

We performed whole-brain tractography using ExploreDTI-4.8.6 (Leemans et al., 2009). Constrained Spherical Deconvolution (CSD) (Tournier et al., 2004) was used to estimate the fiber orientation distribution function. In the tractography algorithm, the seed point resolution $(2 \times 2 \times 2) \ mm^3$, the step size was $1$ mm, the angle threshold was $30^\circ$, and the fiber length range was $50 – 500$ mm.

#### 2.3. Graph generation

We constructed graphs using twenty different graph-construction schemes. We normalized all graphs so that the maximum edge weight in each graph was equal to 1. We also set the elements of the diagonal of all graph matrices equal to 0, since they correspond to connections of a node with itself.

#### 2.3.1. Node definition

We used the Automated Anatomical Labeling (AAL) atlas (Tzourio-Mazoyer et al., 2002) to define the 90 cortical and subcortical areas of the cerebrum that correspond to the nodes of the structural networks. The white matter (WM) tracts linking those areas are the connections, or edges, of the networks. The network generation was performed in ExploreDTI-4.8.6 (Leemans et al., 2009). This process resulted in nine connectivity matrices (CMs) for the data for each diffusion weighting and each scan of each participant. Each CM had edges weighted by a different metric averaged along the corresponding WM tracts. Those metrics are: fractional anisotropy (FA), mean diffusivity (MD), radial diffusivity (RD), number of streamlines (NS), streamline density (SLD), percentage of streamlines (PS), tract volume (TV), tract length (TL) and Euclidean distance between the nodes (ED), and are listed in Table 1.

#### 2.3.2. Integrated graphs

We used the algorithm described by Dimitriadis et al. (2017b, c) to generate an integrated network for the data from each diffusion-weighting and each scan of each participant. Following Dimitriadis et al. (2017b), for each participant at each time point, a two-step

### Table 1

| Metric                        | Abbreviation |
|-------------------------------|--------------|
| Fractional anisotropy         | FA           |
| Mean diffusivity              | MD           |
| Radial diffusivity            | RD           |
| Number of streamlines         | NS           |
| Percentage of streamlines     | PS           |
| Streamline density            | SLD          |
| Tract volume                  | TV           |
| Tract length                  | TL           |
| Euclidean distance between    | ED           |
process was followed:

1) We used the diffusion-distance (Hammond et al., 2013) between individual CMs to maximise information provided by each metric and create a linear-combination (or integrated) graph, and

2) we used an Orthogonal Minimal Spanning Tree (OMST) algorithm (Dimitriadis et al., 2017a, c) to select the edges, so as to maximise the difference (Global Efficiency - Cost), while maintaining the connectivity of the nodes. The benefit of the method lies in the fact that both the topology that results from selecting the edges and the assignment of the edge weights are performed in a data-driven manner, and no arbitrary threshold needs to be imposed. This additionally ascertains that both strong and weak edges are treated equally.

Motivated by the fact that the nine metrics shown in Table 1 exhibit a number of covariances, we also considered integrated graphs formed from subsets of those metrics, to explore whether using fewer variables to define edge-weights has an impact on network reproducibility.

We note here that using linear combinations of metrics as edge weights is motivated by the fact that the transport and integration properties of the brain are affected by more than one attribute of the white matter tracts. Recognizing that, other studies have also used combinations of metrics to weigh the edges. For example, Nigro et al. (2016) used the product of NS and FA to weigh the edges. In addition to using the algorithm of Dimitriadis et al. (2017b), we also constructed networks using the NS, FA or MD as edge weights, due to their prevalent use in the literature (for example Honey et al. (2009) and Collin et al. (2016)), employing the OMST algorithm to select the edges in a data-driven manner.

2.3.3. Single-metric graphs

In addition to using the algorithm of Dimitriadis et al. (2017b), we also constructed networks using the NS, FA or MD as edge weights, due to their prevalent use in the literature (for example Honey et al. (2009) and Collin et al. (2016)), employing the OMST algorithm to select the edges in a data-driven manner.

2.3.4. Thresholded graphs

Finally, we constructed graphs with topology determined by the CM that is weighted by the NS, FA or MD, and a threshold applied to remove edges with the lowest weights. Instead of imposing an arbitrary threshold, the threshold was determined by imposing the constraint that the graphs exhibit the same sparsity as the OMST graphs that exhibited the highest reproducibility (more on this is included in Section 3). Once the topology of each of those graphs was specified, the weights of the edges were either kept as they were or re-weighted with one of the remaining two metrics.

2.3.5. Summary of graphs investigated

The details of all the schemes that we considered are listed in Table 2 for easy reference. In the same table we also list the mean graph similarity (see Section 2.5) between scans for those schemes, for graphs generated from the DWIs with $b = 2000 s/mm^2$, because that guided the decision of which schemes to look into in more detail. We discuss this more in Section 3.

2.4. Graph theory

We computed graph theoretical metrics for all the graphs using the Brain Connectivity Toolbox (Rubinov and Sporns, 2010). Specifically, we calculated the node degree, clustering coefficient, local efficiency and betweenness centrality for each node. We also calculated the global efficiency and the characteristic path length for each graph.

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**Table 2**  
Graph-construction schemes. The first seven schemes are the ones that we discuss in detail in this article. The remaining 13 either give smaller reproducibility or are very similar to one of the first seven and therefore are not discussed in detail - and thus are numbered rather than given an abbreviation.

| Abbreviation | Initial Edge Weights | Topology | Final Edge Weights | Mean Graph Similarity ($b = 2000 s/mm^2$) |
|--------------|----------------------|----------|--------------------|-------------------------------------------|
| NS - OMST    | NS                   | OMST     | unchanged          | 0.918                                     |
| NS + FA OMST | lin. comb. of NS and FA | OMST     | unchanged          | 0.785                                     |
| 9-m OMST     | lin. comb. of all 9 metrics in Table 1 | OMST     | unchanged          | 0.852                                     |
| NS-thr       | NS                   | keep highest-NS edges | re-weight with FA | 0.878                                     |
| NS-t/FA-w    | NS                   | keep highest-NS edges | re-weight with MD | 0.867                                     |
| NS-t/MD-w    | NS                   | keep highest-NS edges | re-weight with NS | 0.887                                     |
| FA-t/NS-w    | FA                   | keep highest-FA edges | re-weight with NS | 0.771                                     |
| 8            | lin. comb. of NS, FA, MD | OMST     | unchanged          | 0.786                                     |
| 10           | lin. comb. of NS, FA, MD, SLD and TL | OMST     | unchanged          | 0.744                                     |
| 11           | lin. comb. of NS, FA, MD, SLD, TL, TV | OMST     | unchanged          | 0.808                                     |
| 12           | lin. comb. of NS, FA, MD, SLD, TL, TV, PT | OMST     | unchanged          | 0.852                                     |
| 13           | lin. comb. of NS, FA, MD, SLD, TL, TV, PT, ED | OMST     | unchanged          | 0.859                                     |
| 14           | FA                   | keep highest-FA edges | re-weight with FA | 0.667                                     |
| 15           | MD                   | keep highest-MD edges | re-weight with NS | 0.559                                     |
| 16           | FA                   | OMST     | unchanged          | 0.558                                     |
| 17           | MD                   | OMST     | unchanged          | 0.473                                     |
| 18           | FA                   | keep highest-FA edges | re-weight with MD | 0.649                                     |
| 19           | MD                   | keep highest-MD edges | re-weight with NS | 0.752                                     |
| 20           | MD                   | keep highest-MD edges | re-weight with FA | 0.554                                     |
2.5. Comparison and statistical analysis

We performed three different forms of comparison:

1. Longitudinal Reproducibility: This was established by comparing the graphs from test and retest data, for each graph-construction scheme, independently for each diffusion weighting.

2. Between-Scheme Agreement: This was assessed by comparing graphs generated via different construction schemes, for each scan and diffusion weighting, for each participant.

3. Inter-B-Value Agreement: This was assessed by comparing graphs generated from the same scan using the same graph-construction scheme, but DWIs with two different diffusion weightings.

2.5.1. Graph reproducibility

The graph similarity between two graphs was computed as the dot product of two vectors, each formed by concatenating the unique edges of each graph, normalized by the magnitudes of those two vectors. Even though it is informative, the similarity between two graphs encompasses both how similar the topologies of the graphs are (i.e. which edges exist in each graph) and how similar the edge weights are. In order to assess the impact of each of these contributions to the overall graph similarity, we looked into each contribution independently.

2.5.2. Topology reproducibility

As a measure for the topology similarity, we constructed a vector containing as many entries as the total number of unique edges in our graphs, and assigned to each entry the value of 1 if the corresponding edge existed in both graphs being compared or if the edge did not exist in either of the graphs being compared, and the value of 0 if the edge in question existed in one of the two graphs being compared but not the other. We then averaged the entries of that vector to get the topology similarity between the two graphs.

2.5.3. Edge reproducibility

In order to assess the edge reproducibility we calculated the intra-class correlation coefficient (ICC) for the edge weights, for all edges that appeared in both scans of at least 12 (one third) of the 37 participants in the group. The choice to use one third as a representative subgroup was partially arbitrary, but motivated by the fact that in order for the ICC to be a sensible measure, it is necessary to have a representative group of participants. We also calculated the absolute value of the fractional difference of the edge weights, namely the absolute value of the difference divided by the mean value of the edge weights, for each edge of each graph. The ICC gives the range of variability of each edge weight between scans in the context of the overall variability of the weights of that edge among participants. On the other hand, the absolute fractional difference gives a participant-specific measure of that variability.

We were also interested in whether dMRI-measured attributes of the WM tracts (for example mean FA, N, etc.) are related to the reproducibility of edge weights. We constructed a general linear model (GLM) with the absolute fractional difference (between scans) of the edge weights as the dependent variable. We hypothesized that the fractional difference between edge weights would depend both on the attributes of the edges and on the absolute difference of those attributes between scans. Additionally, because the values of attributes of WM tracts are highly correlated between scans (a fact confirmed in our analysis, with all WM tract attributes exhibiting correlation coefficients of 0.83 or higher between scans, with p-values of $10^{-7}$ or lower), we used only the attributes listed in Table 1 for graphs generated from the first scan and their differences between scans, as independent variables (all variables were z-transformed). We also wanted to assess whether the edges that appear in the graph from only one of the two scans have any particular attributes. We used two-sample t-tests to compare the distributions of the nine edge attributes for edges that appeared in both scans to their distributions for edges that appeared in only one of the two scans.

2.5.4. Most significant edges

To identify the edges that have the highest weights across participants for each scheme, we selected the edges with weight of 0.9 or higher from the graphs of each participant and summed up the weights. The edges with the highest sums of edge weights were identified as the strongest for each scheme and each scan.

2.5.5. Reproducibility of graph theoretical metrics

To assess the longitudinal reliability of graph theoretical metrics for the different graph-construction schemes, we calculated the ICC and the absolute value of the fractional difference for the graph theoretical metrics between the two scans, both for the local and the global graph theoretical metrics listed in Sec. 2.4.

2.6. Power of structural network analyses

We were interested in evaluating the impact of different graph-construction schemes on the number of participants required in: a) comparative studies, namely studies where groups of participants exhibiting different characteristics (cognitive abilities, disease, etc.) are compared to each other; and b) longitudinal studies, namely studies in which specific measures are computed at two or more different time points for the same participants. A detailed calculation of the number of participants requires knowledge of the specific quantities of interest as well as of the populations involved, therefore such calculations need to be made on a case-by-case basis.

To estimate the impact of the choice of scheme on the power of such studies and on the required number of participants, we assume that we have two populations, each with the same number of participants $N$, and we measure the quantity $x$ for each participant. Alternatively, we have a population with $N$ participants who undergo an intervention, and we measure the quantity $x$ for all participants before and after the intervention. We also assume that the distribution $p_1(x)$ of $x$ for the first population (in the former scenario) or for the population before the intervention (in the latter scenario) is normal with a mean of 0, while for the second population (in the former scenario) or for the population after the intervention (in the latter scenario) the distribution $p_2(x)$ is normal with a mean of $\mu$. Finally, we assume that the standard deviations (SD) of both distributions are equal to each other, and denoted by $\sigma$. As demonstrated by Mumford (2012), if we specify the confidence level at which we wish to detect a possible difference in the means of the distributions, the quantity

$$Q = \sqrt{N\mu/\sigma}$$

(2.1)

determines the power of the study to identify a possible effect. The higher $Q$ is, the higher the power of the study. This means that the tighter the distributions (lower $\sigma$), the lower the number of participants needed to detect the effect. The fact that it is the square root of $Q$ means that even a modest improvement in $\sigma$ can lead to a significant reduction in the number of participants required to detect a given effect with the same power, for a given statistical-significance threshold. On the other hand, an increase in $\sigma$ can lead to a deterioration of the power of a study, if not enough participants can be recruited to allow for confident detection of a given effect. If the number of participants cannot be changed, the dependence of $Q$ on the mean $\mu$ of the second distribution indicates that reducing $\sigma$ implies that a smaller value of $\mu$, and thus of deviation from the zero-mean distribution, is required for the effect to be observed with a given power at a given statistical-significance threshold. Taking this into account, in order to assess the impact of the choice of graph-construction scheme of the various metrics of interest, we calculated the SD of their distributions. We then calculated the increase in the number of participants that would be required, for all the graph-
construction schemes in comparison to the scheme with the lowest SD for the metrics of interest.

2.7. A note on b-values

As mentioned in Sec. 2.1, the DWIs were acquired for three different diffusion weightings. B-values of up to 2000 s/mm² give very good fit for the diffusion tensor (DT) and its fractional anisotropy, while for higher b-values the higher order effects of diffusion need to be taken into account and kurtosis terms need to be included in the fit (Jensen et al., 2005; Jensen and Helpern, 2010; Tabesh et al., 2011). On the other hand, b-values of under 1500 s/mm² can be problematic when it comes to resolving crossing fibers with CSD tractography algorithms (Tuch et al., 2002; Tournier et al., 2004, 2008; Cho et al., 2008), which is important given the prevalence of such fibers in the human brain (Jeurissen et al., 2012). Here, we present the results derived from DWIs acquired with \( b = 2000 \) s/mm² in more detail than for the other weightings, because, unlike the other two diffusion weightings, this one gives reliable tractography results with the CSD algorithm and reliable results for the DT fits. It is, however, important to understand how similar or different the results are for the other two diffusion weightings in comparison to \( b = 2000 \) s/mm², specifically for single-shell experiments or datasets as will be discussed in Sec. 4. We therefore also present the reproducibility results for those two diffusion weightings.

2.8. Data and code availability

The HCP test-retest data is freely available as listed above. The code used to generate the graphs for the structural brain networks with the OMST schemes is available at: https://github.com/stdimitr/multi-group-p-analysis-OMST-GDD. The code used to perform the reproducibility analysis is not freely available, but is based exclusively on Matlab functions. This adheres to the data and code requirements of our funders.

3. Results

As explained in Sec. 2, we considered twenty graph-construction schemes (see Table 2). We present detailed results for the seven schemes that (a) resulted in reproducibility (for the graphs and their various attributes) that is high enough for the graphs to be useful for comparative and longitudinal studies and b) are different enough from each other to convey a different picture of the structural connectome. Specifically, we excluded all schemes that resulted in mean graph similarity over participants of under 0.75 (schemes 10, 14, 15, 16, 17, 18 and 20 in Table 2; also see Messaritaki et al. (2019) for more details on the graph similarity for the FA- and MD-schemes). We also excluded schemes for which the graph similarity was under 0.7 for any of the participants regardless of the mean graph similarity (schemes 8, 9, 19 in Table 2). Schemes 11, 12 and 13 resulted in graphs that are very similar to the 9-m OMST scheme, and we decided to discuss the latter in detail due to the fact that it exhibits higher reproducibility for the graph theoretical metrics. Based on these considerations, the schemes we discuss in detail and the abbreviations used to refer to them, are:

- Scheme 1: The edge weights are equal to the NS, and the OMST algorithm is used to select the edges (NS-OMST).
- Scheme 2: The edge weights are equal to a linear combination of the NS and the FA, with the coefficients identified by the diffusion-distance algorithm. The OMST algorithm is used to select the edges (NS + FA OMST). This is the same scheme that is described by Dimitriadis et al. (2017b), using only two metrics to weigh the edges.
- Scheme 3: The edges are weighted by linear combinations of 9 metrics, with the coefficients identified via the diffusion-distance algorithm. The OMST algorithm is used to select the edges (9-m OMST).
- Scheme 4: The edges are weighted by the NS, and an absolute threshold is used to keep the edges that have the highest NS (NS-thr).
- Scheme 5: The edges are first weighted by the NS and thresholded to keep the ones with the highest NS. Then they are re-weighted by their FA. In other words, the topology of the graph is defined by the thresholded-NS scheme and the weights are equal to the FA (NS-t/FA-w).
- Scheme 6: The edges are first weighted by the NS and thresholded to keep the ones with the highest NS. Then they are re-weighted by their MD. In other words, the topology of the graph is defined by the thresholded-NS scheme and the weights are equal to the MD (NS-t/MD-w).
- Scheme 7: The edges are first weighted by the FA and thresholded to keep the ones with the highest FA. Then they are re-weighted by their NS. In other words, the topology of the graph is defined by the thresholded-FA scheme and the weights are equal to the NS (FA-t/NS-w).

We remind the reader that, for the four thresholded schemes, the threshold was defined so that the networks exhibited the same sparsity as the corresponding 9-m OMST networks, which had the highest mean network similarity of the OMST networks that use more than one metric (see Sec. 3.2.1).

3.1. Representative graphs

Fig. 1 shows the graphs for the structural networks of the first scan of one participant for the seven different schemes, derived from DWIs acquired with \( b = 2000 \) s/mm².

For six of the seven graph-construction schemes the majority of the edges close to the diagonal were non-zero. The graph resulting from the FA-t/NS-w scheme was the only exception, in which the edges close to the diagonal for nodes up to node 30 were not present, or not as strong in relation to the rest of the edges as for the other schemes.

The weights of the edges were very variable between schemes, as was the relative weight of the edges within each scheme. For the NS-OMST and NS-thr schemes, which rely exclusively on the NS for the topology and edge weights, only a few edges had weights close to 1, while all the others had weights of 0.6 or lower. For the NS-t/MD-w graph, on the other hand, most edges had values close to 1, reflecting the fact that the MD of white matter tracts is quite uniform in the human brain. The remaining four schemes exhibited a more uniform distribution of edge weights between the values of 0 and 1.

3.1.1. Between-scheme similarity of graphs

The mean of the graph similarity between schemes (over the 37 participants and the two scans) is given in Table 3 for all pairs of graph-construction schemes. The high similarity of the graphs generated by the NS-t/FA-w and NS-t/MD-w schemes is, of course, a result of their topologies being identical. The graphs generated by the NS-OMST and NS-thr schemes were also highly similar to each other, which is due to the fact that the weights used for the edges are the same. Notably, this is true despite of the fact that these graphs generally exhibited very different sparsities (the mean sparsity of the NS-OMST graphs across participants was 0.044 while that of the NS-thr graphs was 0.096.)

3.2. Reproducibility results

3.2.1. Graph reproducibility

The between-scan graph similarity for the 37 participants is shown in Fig. 2. We show the similarity for the graphs constructed via the OMST schemes separately from that for the four thresholded schemes, using the same scale on the vertical axis in both plots.

The NS-OMST had the highest graph similarity among the OMST schemes, just over 0.9 for most participants. Of the seven schemes considered, the NS-thresholded scheme resulted in the highest similarity, about 0.95 for all participants. Notably, even though the FA-t/NS-w scheme resulted in a very high mean graph similarity, it also resulted
OMST graph is the sparsest, while the other graphs have the same sparsity as each other. The colors in the colorbar correspond to the edge weights. By construction, the NS-similarity are indicated in bold letters.

The mean and SD of the graph similarity for the three different schemes, indicating that the graph similarities are not affected by the diffusion weightings. The NS-thr, NS-t/FA-w and NS-t/MD-w schemes all have the highest mean and the smallest SD of topology similarity for all three diffusion weightings.

We also compared the distributions of graph similarity for graphs generated with two different schemes separately for each diffusion weighting, for all possible pairs of schemes (paired t-tests, after FDR multiple comparison correction with a threshold of \( p < 0.01 \)). The results are shown in Table 5, where the values indicate pairs of distributions that are statistically significantly different from each other. There are no statistically significant differences in the similarity distributions between \( b = 2000 \text{ s/mm}^2 \) and \( b = 3000 \text{ s/mm}^2 \) for any of the seven schemes, indicating that the graph similarities are not affected by the \( b \)-value for those stronger diffusion weightings. Additionally, the 9-m OMST scheme does not show any statistically significant differences in the similarity distributions regardless of the pair of \( b \)-values compared. It is possible that using several metrics to weigh the edges reduces the effect of inaccuracies in the evaluation of tract metrics, and therefore makes that scheme more robust across \( b \)-values, as far as the graph similarity is concerned.

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3.2.2. Topology reproducibility

The topology similarity is shown in Fig. 3 for the different schemes for \( b = 2000 \text{ s/mm}^2 \). The mean and the SD of the topology similarity for each scheme are given in Table 7, for the three diffusion weightings. The topology similarity was over 0.9, for all participants regardless of the scheme used to construct the graphs. The NS-OMST scheme had the highest mean and the smallest SD of topology similarity for all three diffusion weightings. The NS-thr, NS-t/FA-w and NS-t/MD-w schemes all

| Table 3 | Mean between-scheme similarity of graphs, for \( b = 2000 \text{ s/mm}^2 \). The mean is over all participants and then over the two scans. The highest values of the similarity are indicated in bold letters. |
|---------|----------------------------------------------------------------------------------|
|          | NS + FA OMST 0.633                                                              |
| 9-m     | OMST                                                          0.637 0.617                                                    |
| NS-thr  | 0.883 0.754 0.744                                                             |
| NS-t/FA-w | 0.538 0.696 0.685 0.808                                                 |
| NS-t/MD-w | 0.537 0.664 0.694 0.798 0.988                               |
| FA-t/NS-w | 0.552 0.539 0.427 0.637 0.503 0.438                                      |

Fig. 1. Sample graphs representing the structural connectome for the first scan of one of the participants, derived from the DWIs with \( b = 2000 \text{ s/mm}^2 \). All graphs have been normalized so that the maximum edge weight within each graph is 1. The colors in the colorbar correspond to the edge weights. In the widest range of graph similarity among the 37 participants, ranging from 0.75 to 0.95.

The mean and SD of the graph similarity for the three different diffusion weightings is given in Table 4. The values of the mean similarity were very close to each other for the graphs generated with the same scheme across \( b \)-values, for all seven schemes. We compared the distributions of the graph similarity for each scheme for all pairs of the three diffusion weightings with paired t-tests, and applied false-discovery-rate (FDR) multiple comparison correction with a threshold of \( p < 0.01 \). The results are shown in Table 5, where “X” indicates pairs of distributions that are statistically significantly different from each other. There are no statistically significant differences in the graph similarity distributions between \( b = 2000 \text{ s/mm}^2 \) and \( b = 3000 \text{ s/mm}^2 \) for any of the seven schemes, indicating that the graph similarities are not affected by the \( b \)-value for those stronger diffusion weightings. Additionally, the 9-m OMST scheme does not show any statistically significant differences in the similarity distributions regardless of the pair of \( b \)-values compared. It is possible that using several metrics to weigh the edges reduces the effect of inaccuracies in the evaluation of tract metrics, and therefore makes that scheme more robust across \( b \)-values, as far as the graph similarity is concerned.

We also compared the distributions of graph similarity for graphs generated with two different schemes separately for each diffusion weighting, for all possible pairs of schemes (paired t-tests, after FDR multiple comparison corrections at a threshold of \( p = 0.01 \)). The results are shown in Table 6. Blank cells indicate pairs of schemes for which the distributions are statistically significantly different for all three \( b \)-values. The numbers in the filled cells indicate the \( b \)-values for which the graph similarity distributions are statistically significantly different for the two higher diffusion weightings. The numbers in the filled cells indicate the \( b \)-values for which the graph similarity distributions are statistically significantly different for the two higher diffusion weightings.

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shows the percentage of edges versus ICC for the seven schemes, with the full range of values for each scheme. The FA-t/NS-w scheme resulted in the highest percentage, 66.4%, of edges with ICCs of 0.85 or higher, while the NS-thr and NS-t/FA-w schemes had 61% and 61.4% edges with ICCs greater than 0.85 respectively. It is noteworthy that the 9-m OMST schemes resulted in distributions that are shifted to lower values compared to those of the other six schemes. That is possibly due to the fact that the nine WM tract metrics that are combined to form the edge weights result in some added variability that leads to lower ICCs.

had the same topology similarity since they share the same topology.

We compared the distributions of the topology similarity for the five schemes (omitting the NS-t/FA-w and NS-t/MD-w because they have the same topology as the NS-thr scheme) with paired t-tests, for each diffusion weighting. For all three diffusion weightings, all pairs of schemes exhibited statistically significantly different distributions of topology similarity (all \( p < 10^{-6}\), and survived FDR multiple comparison corrections for a \( p \)-value threshold of 0.01), indicating that the topology similarity is dependent on the chosen scheme.

### 3.2.3. Edge reproducibility

The ICC for the edge weights is shown in Fig. 4, for graphs generated from the DWIs acquired with \( b = 2000\) s/mm\(^2\). For all except the 9-m OMST scheme, the majority of the edge weights exhibited ICCs above 0.7. In order for the plots in Fig. 4 to be easily interpretable, the scale was set to be between 0 and 1 and therefore the few edges that have ICCs less than zero, i.e., edges for which the between-scan variability of the edge-weights is larger than the range of values of those weights, are not evident. Fig. 5 shows the percentage of edges versus ICC for the seven schemes, with the full range of values for each scheme. The FA-t/NS-w scheme resulted in the highest percentage, 66.4%, of edges with ICCs of 0.85 or higher, while the NS-thr and NS-t/FA-w schemes had 61.9% and 61.4% edges with ICCs greater than 0.85 respectively. It is noteworthy that the 9-m OMST schemes resulted in distributions that are shifted to lower values compared to those of the other six schemes. That

### Table 4

|           | NS OMST | NS + FA OMST | 9-m OMST | NS-thr | NS-t/FA-w | NS-t/MD-w | FA-t/NS-w |
|-----------|---------|--------------|----------|--------|-----------|-----------|-----------|
| \( b = 1000\) s/mm\(^2\) | mean    | 0.901        | 0.763    | 0.852  | 0.952     | 0.862     | 0.845     | 0.855     |
|           | SD      | 0.020        | 0.034    | 0.026  | 0.010     | 0.022     | 0.023     | 0.045     |
| \( b = 2000\) s/mm\(^2\) | mean    | 0.918        | 0.785    | 0.852  | 0.962     | 0.878     | 0.867     | 0.888     |
|           | SD      | 0.021        | 0.028    | 0.023  | 0.008     | 0.018     | 0.020     | 0.041     |
| \( b = 3000\) s/mm\(^2\) | mean    | 0.917        | 0.779    | 0.847  | 0.923     | 0.878     | 0.865     | 0.882     |
|           | SD      | 0.023        | 0.025    | 0.025  | 0.009     | 0.021     | 0.023     | 0.051     |

### Table 5

Comparison of similarity distributions across \( b \)-values (paired t-tests). The cells marked with X indicate the pairs of \( b \)-values for which the distributions were statistically significantly different, after FDR correction for multiple comparisons has been applied, at a \( p \)-value threshold of 0.01.

|           | 1000 s/mm\(^2\) vs. 2000 s/mm\(^2\) | 1000 s/mm\(^2\) vs. 3000 s/mm\(^2\) | 2000 s/mm\(^2\) vs. 3000 s/mm\(^2\) |
|-----------|-------------------------------------|-------------------------------------|-------------------------------------|
| NS OMST   | X                                   | X                                   | X                                   |
| NS + FS OMST | X                               |                                      |                                      |
| 9-m OMST  | X                                   |                                      |                                      |
| NS-thr    | X                                   | X                                   | X                                   |
| NS-t/FA-w | X                                   | X                                   | X                                   |
| NS-t/MD-w | X                                   |                                      |                                      |
| FA-t/NS-w | X                                   |                                      |                                      |

### Table 6

Comparison of distributions of network similarity across schemes, for the 3 \( b \)-values (paired t-tests, followed by FDR multiple-comparison correction with \( p \)-value threshold of 0.01). Blank cells indicate pairs of schemes for which the distributions are statistically significantly different for all three \( b \)-values. The numbers in the filled cells indicate the \( b \)-values (in s/mm\(^2\)) for which the similarity distributions are not statistically significantly different.

|           | NS + FA | 9-m OMST | NS-thr | NS-t/FA-w | NS-t/MD-w |
|-----------|---------|----------|--------|-----------|-----------|
| NS-thr    | 1000    |          |        |           |           |
| NS-t/FA-w | 1000    |          |        |           |           |
| FA-t/NS-w | 1000    | 1000, 2000, 3000 | 1000, 2000, 3000 | 1000, 2000, 3000 |
| NS OMST   | NS + FA | 9-m OMST | NS-thr | NS-t/FA-w | NS-t/MD-w |
|           |         |          |        |           |           |
We note that these percentages are correct for the graphs generated from the DWIs with $b = 2000 \text{s/mm}^2$. However, the conclusions about which schemes do better also hold for the graphs generated from the DWIs with $b = 1000 \text{s/mm}^2$ and $b = 3000 \text{s/mm}^2$, and the distributions shown in Figs. 5 and 6 were very similar for those two $b$-values.

The results of the GLM analysis (see Sec. 2) are given in Table 8. For the NS-OMST, NS + FA OMST and NS-thr schemes, the absolute difference in the number of streamlines of the edge between the two scans was the most significant predictor variable, and the larger the absolute difference in NS, the larger the absolute fractional difference in edge weights. For the NS-OMST scheme, the tract volume explained some of the variability, with the negative regression coefficient indicating that the smaller the volume of a tract, the larger the absolute fractional difference in edge weights. For the NS-thr scheme, the number of streamlines in the first scan was also significantly and negatively correlated with the absolute fractional difference in edge weight. In other words, edges that have a small number of streamlines are less reliably reproduced. For the NS-t/FA-w and NS-t/MD-w schemes, the absolute difference (between scans) in the metric used to weigh the edges was the best predictor, and positively correlated with the edge-weight absolute fractional difference. Finally, and somewhat surprisingly, for the FA-t/NS-w scheme, the best predictor variable was the TV in the first scan, with the absolute difference in TV between scans also contributing. For the 9-m OMST scheme, only a small fraction of the variability was explained by the attributes of the edges, and the coefficients of the GLM, even though statistically significant, were very small (less than 0.1) and therefore not useful in predicting which edges are likely to be highly

### Table 7

Mean and SD of the topology similarity distributions of the graphs for the 3 $b$-values.

|        | NS OMST | NS + FA | 9-m OMST | NS-thr | NS-t/FA-w | NS-t/MD-w | FA-t/NS-w |
|--------|---------|---------|----------|--------|-----------|-----------|-----------|
| $b$: 1000 s/mm$^2$ | mean 0.981 | 0.944 | 0.966 | 0.973 | 0.973 | 0.973 | 0.931 |
|        | SD 0.003 | 0.008 | 0.005 | 0.004 | 0.004 | 0.004 | 0.009 |
| $b$: 2000 s/mm$^2$ | mean 0.984 | 0.947 | 0.962 | 0.974 | 0.974 | 0.974 | 0.934 |
|        | SD 0.002 | 0.007 | 0.007 | 0.005 | 0.005 | 0.005 | 0.011 |
| $b$: 3000 s/mm$^2$ | mean 0.983 | 0.947 | 0.962 | 0.974 | 0.974 | 0.974 | 0.934 |
|        | SD 0.003 | 0.005 | 0.006 | 0.005 | 0.005 | 0.005 | 0.010 |

**Fig. 3.** Topology similarity between the two scans for the 37 participants, for $b = 2000 \text{s/mm}^2$. For clarity of the plot, the similarity for the OMS schemes is plotted separately from that for the thresholded schemes, however both plots use the same scale for ease of comparison. The NS-thr, NS-t/FA-w and NS-t/MD-w schemes share the same topology, and therefore the same topology similarities, and therefore the markers for all three schemes are co-located in the plot.

**Fig. 4.** ICC of the edges present in both scans of at least 12 of the 37 participants, for the different schemes considered.
reproducible. That could be due to the fact that the linear combination of metrics used to weigh the edges in the graphs is different among participants.

The comparison of the distributions of edge attributes between edges that appear in graphs from both scans and those that appear in graphs from only one of the two scans showed no statistically significant differences. However, the edges that appear in graphs from only one of the two scans generally had low NS and low TV, for all graph-construction schemes except the FA-t/NS-w. This is shown in Figs. 7 and 8, where it is also evident that for the NS-OMST, NS-thr and FA-t/NS-w schemes, edges with low NS but large differences in the NS between scans exhibited the largest absolute fractional differences in edge weights. We note that these two figures show edges that appear in the graphs representing the networks, i.e. edges that have survived the graph-construction process.

### 3.2.4. Strongest edges

The edges that are the strongest in all participants depended on the scheme used. The AAL regions interconnected by those edges are listed in Table 9 for the seven graph construction schemes.

### 3.2.5. Reproducibility of graph theoretical metrics

Table 8 GLM for the absolute value of the fractional difference of edge weights, for edges that appear in both scans of a given participant. The $p$-values for all the coefficients shown here were smaller than $10^{-50}$, and they all survived FDR multiple comparison correction. The variables are listed in order of significance.

| variables         | NS OMST | NS + FA OMST | NS-thr | NS-t/FA-w | NS-t/MD-w | FA-t/NS-w |
|-------------------|---------|--------------|--------|-----------|-----------|-----------|
| $\Delta$(NS)      | 0.63    | 0.55         | 0.73   | 0.71      | 0.41      | 0.60      |
| TV                | -0.50   | -0.22        | -0.46  | -0.22     | -0.60     | -0.39     |

| % variability explained | 39.2 | 33.2 | 48.1 | 57.2 | 16.5 | 31.7 |

Fig. 5. Percentage of edges versus ICC, for $b = 2000$ s/mm². Left panel: OMST schemes, right panel: thresholded schemes. Only edges that show up in the graphs from both scans of at least 12 participants have been included.

Fig. 6. Percentage of edges versus absolute fractional difference in the edge weights in the graphs from the two scans, for $b = 2000$ s/mm². Left panel: OMST schemes, right panel: thresholded schemes. The points at the rightmost side of each figure correspond to absolute fractional difference of 2, namely to edges that appear in graphs from only one of the two scans.

The four local graph theoretical metrics: node degree, clustering coefficient, betweenness centrality and local efficiency. The NS-thr scheme resulted in the ICC distributions with the highest mean for all these metrics, with the distributions also appearing the tightest around the mean (the only possible exception being the distribution for the betweenness centrality of the NS OMST scheme). The NS-t/FA-w and NS-t/MD-w schemes also resulted in high ICCs for the node degree and the clustering coefficient.

Fig. 10 shows the distributions of the absolute value of the fractional difference between the two scans for the same graph theoretical metrics, for the seven schemes. The 9-m OMST scheme had the lowest mean values and very tight distributions around those means, for all four node-level graph theoretical metrics considered. It is noteworthy that most schemes resulted in comparable distributions for the absolute fractional differences, with the FA-t/NS-w scheme and the NS OMST scheme for the case of the local efficiency and the clustering coefficient, being the exceptions.

The ICCs and mean absolute fractional differences of the global efficiency and the characteristic path length are given in Table 10. Most schemes resulted in low values for the mean absolute fractional differences, however the ICCs for both the global efficiency and the characteristic path length were above 0.85 only for the schemes that rely exclusively on the NS to construct the graphs.
Consider a study that aims to evaluate whether an intervention performed in a group of participants results in an overall change in their structural networks. Assume that the group is split into two subgroups with equal number of participants $N$, with the intervention performed in only one of the two groups, for example group 2, and no intervention is performed on group 1.

3.3. Power of structural network studies

3.3.1. Impact on graph changes

The graphs before and after the intervention are constructed based on a given scheme and the graph similarities are calculated. The distributions of the graph similarities for the two groups will have different means, differing by $\mu$, and the same SD $\sigma$. For the dataset used in this work, the NS-thr scheme resulted in the graph similarity distribution with the lowest SD (Table 4). Table 11 shows the ratio of the SD for the graph similarity distribution of each scheme over the SD of the NS-thr scheme, as well as the factor by which the number of participants...
Table 9

Connections that are strongest for all participants for the seven graph construction schemes.

| Areas Connected (AAL atlas) | Schemes                      |
|-----------------------------|------------------------------|
| L. superior frontal gyrus  | NS-OMST; (NS + FA)-OMST      |
| R. superior frontal gyrus  | NS-OMST; (NS + FA)-OMST      |
| R. medial frontal gyrus    | 9-m OMST; NS-thr             |
| L. supplementary motor area | (NS + FA)-OMST; 9-m OMST; FA-|
| R. supplementary motor area | t/NS-w                       |
| L. hippocampus - L. thalamus| NS-t/MD-w                   |
| R. hippocampus - R. thalamus| NS-t/MD-w                   |
| L. hippocampus - R. hippocampus| NS-t/MD-w                  |
| L. hippocampus - L. amygdala| NS-t/MD-w                   |
| R. hippocampus - R. amygdala| NS-t/MD-w                   |
| L. putamen - L. globus pallidus| NS-thr                     |
| R. putamen - R. globus pallidus| NS-thr                   |
| L. posterior cingulate gyrus - L. superior occipital gyrus| NS-t/FA-w               |
| R. posterior cingulate gyrus - R. superior occipital gyrus| NS-t/FA-w               |
| L. cuneus - R cuneus       | NS-t/FA-w                   |
| R. calcarine sulcus - L. superior occipital gyrus| NS-t/FA-w               |
| R. cuneus - L. superior occipital gyrus| NS-t/FA-w               |

The distributions (over the 90 nodes of each graph) of the SDs of the local graph theoretical metrics for data acquired with $b = 2000$ s/mm$^2$ are shown in Fig. 11. The distributions of the SDs for the betweenness centrality are given in a logarithmic scale. The scheme that exhibits the lowest SD for different graph theoretical metrics depends on the metric itself, and that prevents us from giving a recommendation on the best scheme to use for all these metrics. However, both the 9-m OMST and the NS-thr schemes result in small SDs for these metrics, so would be good choices.

Table 12

3.4. Comparison of graphs resulting from different diffusion weightings

As noted earlier, DWIs acquired with different diffusion weightings have different benefits and drawbacks as far as parameter fit, tractography results, etc. are concerned. It is important to understand whether the graphs generated through the same scheme using DWIs acquired with different diffusion weightings are similar to each other. Fig. 12 shows the graph similarity for the three pairs of b-values compared.

In most cases, the graphs generated from DWIs of different b-values were very similar to each other, with values of the graph similarity of above 0.8. The FA-t/NS-w scheme exhibited very variable graph similarity between different b-values, in particular between $b = 1000$ s/mm$^2$ and $b = 3000$ s/mm$^2$. This is likely the result of the fact that the FA, which is used to define the topology in that scheme, is not as reliably measured with the DWIs of $b = 3000$ s/mm$^2$ as it is with DWIs of smaller b. Of the OMST schemes, the NS + FA scheme had the lowest graph similarity between graphs constructed with data acquired at different b-values. The highest similarity was exhibited by the NS-thr graphs.

Fig. 9. ICCs for the local graph theoretical metrics ($b = 2000$ s/mm$^2$). In each box, the middle line shows the mean of the distribution, the edges of the box represent the 25% and 75% points, and the circles indicate points that are thought to be outliers. Each distribution is over the 90 nodes of the graph.
4. Discussion

We presented a study on the reproducibility of graphs and their various attributes for different graph-construction schemes, for structural brain networks in the human brain, using the HCP test-retest data. The key findings of our work have implications on longitudinal and comparative studies, as well as on studies that combine dMRI data collected with different diffusion weightings. They are as follows:

1. Different graph-construction schemes result in networks with distinct topologies and edge weights. Even though not surprising, this is an important point because the structural connectome supports function in the brain (Bassett and Gazzaniga, 2011; Mill et al., 2017) and connections between nodes in structural networks can be used to understand the mechanisms that underlie functional connectivity. This is relevant not only for whole-brain studies, but also, and maybe even more so, for studies that use structural sub-networks to study the human brain (for example Drakesmith et al. (2015)).

2. The reproducibility of the graphs depends on the graph construction scheme, with some schemes exhibiting mean similarity of the order of 0.9 or higher while others falling in the range of about 0.8. For the data used in this study, the NS-thr scheme gave the highest mean graph similarity, for all three diffusion weightings. Additionally, the SD of the graph similarity depends on the graph-construction scheme used. Knowing both the mean and the SD of the similarity distribution for healthy participants in the absence of ageing or intervention is essential, because it allows one to make reliable predictions for the number of participants required to observe changes in structural brain networks in developmental, intervention or patient studies.

3. The reproducibility of the topology of graphs depends on the graph construction scheme. The NS-OMST scheme gave the highest topological reproducibility, for all three diffusion weightings. This is in contrast to the fact that the NS-thr scheme resulted in the highest reproducibility for the weighted graphs, and implies that studies which focus on the topology of structural networks rather than on the specific weights of the edges, or studies which use binary rather than weighted networks, may benefit from using different schemes to construct the graphs representing the structural networks.

4. The graphs constructed from DWIs of different diffusion weightings exhibit very good similarity with each other, for most schemes. Of the schemes we investigated in this work, the schemes that rely exclusively on the NS are the most reliable across diffusion weightings. The good similarity implies that each specific combination of algorithms used to fit the DT, perform the tractography and construct the graphs, reveals a fairly consistent picture of the structural connectome, regardless of the diffusion weighting used to acquire the data. The only possible exception is the FA-t/NS-w scheme, which results in

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Table 10
ICCs and mean absolute fractional differences for the global efficiency and the characteristic path length, for the different schemes, for $b = 2000 \text{s/mm}^2$.

|                  | NS OMST | NS + FA OMST | 9-m  | NS-thr | NS-t/FA-w | NS-t/MD-w | FA-t/NS-w |
|------------------|---------|--------------|------|--------|-----------|-----------|-----------|
| $E_{glob}$       | ICC     | 0.86         | 0.23 | 0.64   | 0.87      | 0.58      | 0.64      | 0.50      |
| char path length | ICC     | 0.86         | 0.30 | 0.72   | 0.87      | 0.51      | 0.57      | 0.79      |
|                  | [frac. diff.] | 0.076       | 0.031| 0.059  | 0.077     | 0.063     | 0.064     | 0.173     |
|                  | [frac. diff.] | 0.068       | 0.068| 0.087  | 0.084     | 0.080     | 0.084     | 0.131     |

Table 11
Ratio of SD of graph similarity distribution for a given scheme over the SD for the NS-thr scheme. Also given is the increase in the number of participants required to achieve the same power of identifying a difference between populations, assuming normal distributions with different means.

|                  | NS OMST | NS + OMST | 9-m  | NS-t/FA-w | NS-t/MD-w | FA-t/NS-w |
|------------------|---------|-----------|------|-----------|-----------|-----------|
| ratio of SDs     | 2.54    | 3.36      | 2.77 | 2.21      | 2.48      | 5.58      |
| required increase in number of participants | 6.5 | 11.3 | 7.7 | 4.9 | 6.2 | 31.2 |

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Fig. 10. Absolute fractional differences between the two scans, for the local graph theoretical metrics ($b = 2000 \text{s/mm}^2$). In each box, the middle line shows the mean of the distribution, the edges represent the 25% and 75% points, and the circles indicate points that are thought to be outliers. Each distribution is over the 90 nodes of the graph.
graphs that exhibit large deviations from each other, in particular between diffusion weightings of $b = 1000 \text{s/mm}^2$ and $b = 3000 \text{s/mm}^2$, with the graph similarity reaching values of under 0.65 for several participants. This could be due to the limited validity of the DT formalism for $b$-values above 2000 s/mm$^2$, in combination with the limited capability of DWIs with $b = 1000 \text{s/mm}^2$ to give good tractography results for crossing fibers. The NS + FA OMST scheme also shows limited reliability when comparing graphs generated from DWIs with $b = 1000 \text{s/mm}^2$ and $b = 3000 \text{s/mm}^2$. This also argues for a possible role that the limited accuracy of the calculation of the FA for larger $b$-values plays in the reproducibility of those graphs across diffusion weightings.

5. The weights of edges that show up in the graphs from both scans of participants were more reliably reproduced for the 9-m OMST, NS-t/FA-w and NS-t/MD-w schemes. The GLM analysis revealed that the absolute difference in edge weights between scans correlates with the graph similarity reaching values of under 0.65 for several participants. This could be due to the limited validity of the DT formalism for $b$-values above 2000 s/mm$^2$, in combination with the limited capability of DWIs with $b = 1000 \text{s/mm}^2$ to give good tractography results for crossing fibers. The NS + FA OMST scheme also shows limited reliability when comparing graphs generated from DWIs with $b = 1000 \text{s/mm}^2$ and $b = 3000 \text{s/mm}^2$. This also argues for a possible role that the limited accuracy of the calculation of the FA for larger $b$-values plays in the reproducibility of those graphs across diffusion weightings.

6. The reproducibility of graph theoretical metrics depends on the graph construction scheme. The NS-thr, NS-t/FA-w and NS-t/MD-w schemes resulted in the ICC distributions over nodes with the highest means. The 9-m OMST scheme resulted in the lowest mean for the distributions of the absolute fractional differences of the node degree, clustering coefficient and the local efficiency, also resulting in a very tight distribution for the 90 nodes. The results held for the graphs constructed using the DWIs of different diffusion weightings. For the global graph theoretical metrics, the NS-OMST and NS-thr schemes exhibited the highest ICCs, while the NS + FA-OMST scheme exhibited the lowest mean absolute fractional differences.

In addition to these important findings, we showed the effect that a non-optimal choice of scheme can have on the power of studies to detect differences in populations or effects of interventions. Our analysis makes it clear that a careful assessment of the impact of schemes on the SDs of various metrics can guide the choice of scheme. Since each scheme has its own strengths and weaknesses, such an analysis can also allow a considered choice of metrics to look at, possibly excluding metrics that have distributions with large SDs and therefore will not be sufficiently informative or powerful. In addition to saving time and resources, this can reduce the need for multiple comparison corrections, further strengthening the analyses.

The differences in the longitudinal reproducibility of the graphs are, to a large extent, due to the fact that they employ different tract metrics to generate the topology and to weigh the edges, and those metrics exhibit different reproducibility across the two scans. Fig. 13 shows a grid on the plane of a tract metric (NS, FA or MD) in scan 1 versus the same tract metric in scan 2, where the color of each grid point reflects the logarithm of the number of connections that exhibit that pair of metrics. This number of connections is a sum of all white matter tracts that result from the tractography (and not only the edges that are present after graph construction) and over all participants. The distribution of NS in scan 1 versus NS in scan 2 is very tight around the equal-value line, indicating high consistency between the values of NS across the two scans. Therefore, tracts are similarly likely or unlikely to be present in the graphs generated from the two scans, for construction schemes that

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### Table 12

| Metric                        | NS OMST | NS + FA OMST | 9-m | NS-thr | NS-t/FA-w | NS-t/MD-w | FA-t/NS-w |
|-------------------------------|---------|--------------|-----|--------|-----------|-----------|-----------|
| $|d_{gini}$ | S1 0.013 | 0.007 | 0.025 | 0.014 | 0.023 | 0.028 | 0.006 |
| | S2 0.011 | 0.009 | 0.014 | 0.011 | 0.025 | 0.030 | 0.006 | 0.002 |
| | S1 0.002 | 0.004 | 0.009 | 0.003 | 0.008 | 0.009 | 0.009 | 0.002 |
| | S2 0.002 | 0.004 | 0.006 | 0.003 | 0.008 | 0.009 | 0.009 | 0.002 |
employ the NS to define the topology. On the other hand, despite the fact that the vast majority of tracts have highly consistent values of FA and MD across the two scans, there are tracts for which these values differ substantially. Therefore, tracts are not equally likely to survive in the graphs of both scans after graph construction, if the FA or MD are used to define the network topology. Even though the number of tracts with FA or MD values that differ significantly is very small compared to the total number of the tracts, it is enough to result in the lower reproducibility of the graphs. This clarifies why graph construction schemes that are based exclusively on NS do better as far as their longitudinal reproducibility goes, compared to scans that incorporate other metrics as well.

Despite the fact that NS-based schemes do better at graph and topology reproducibility, and as was explained in Sec. 2.3.2, the transport and integration properties of the brain are affected by more than one attribute of the white matter tracts, and therefore considering metrics other than the NS is essential in structural brain network studies. More generally, the graph construction method that results in the highest reproducibility is not necessarily the one that best reflects the functional organization of the brain. In fact, different schemes could be closer to the truth for different brain functions, and most appropriate to answer different research questions. This should be taken into account, and the choice of scheme should ideally be balanced between minimizing variability among participants and being sensitive to true changes due to maturation.

Our results go some way into proving why different studies lead to incongruent conclusions for the network characteristics of patient populations or for the developmental or interventional changes observed in structural brain networks. Even if they use the same acquisition protocols and diffusion weightings for data collection, studies that use different schemes to construct the graphs representing the structural networks are bound to give different results for the topologies and for the significance of the edges. They are also bound to exhibit different reproducibility for the graph theoretical metrics and therefore different capability to observe changes or differences in those. In other words, each scheme is “tuned into” specific graph theoretical metrics and is best suited to detect differences or changes in those.

One of the main goals of brain network analyses is to understand the structural underpinnings of the functional organization of the human brain. Functional networks generated from magnetoencephalography or electroencephalography data have revealed that the strength of functional connections between brain areas depends on the frequency of the signals (Brookes et al., 2011; Deco et al., 2017; Messaritaki et al., 2017;
Additionally, they have shown that there may be more than one mechanism of coupling between brain areas, such as phase-phase, phase-frequency, phase-amplitude and amplitude-amplitude (Hyafl et al., 2015; Dimitriadis et al., 2015, 2018; Dimitriadis and Salis, 2017; Dimitriadis, 2018). Given the distinct mechanisms that the different frequencies and ways of coupling imply, it is possible that different characteristics of the WM tracts support each mechanism. Therefore, different graph construction schemes could result in structural network graphs that have higher overlap with the different functional networks, and can therefore be better suited to understand the corresponding mechanisms (Tewarie et al., 2019). This point is further solidified by our finding that different edges appear to be strongest for each graph-construction scheme.

Our study has a few limitations which we now discuss. The main limitation is that the specific results relating to the optimal scheme to use apply specifically to the HCP dataset we used, and cannot be generalized to other datasets that may involve different scanners or acquisitions, or to analysis strategies that involve different tractography algorithms. The point is clear, however, that it is very much worth looking into the optimal scheme for graph construction for each study, because such an investigation can yield a significant gain in the power of the study. Additionally, the reproducibility was assessed on the basis of two scans. Three or more scanning sessions would give a more robust assessment of the reproducibility. Furthermore, scanning the participants in a controlled manner, making sure that they are scanned at the same time of day, for example, would also be desirable. Also, our thresholded networks used a threshold so that their sparsity is the same as the sparsity of the OMST networks. Different thresholds could lead to different results for the reproducibility of the graphs and their attributes for those schemes, and could also be worth exploring. Lastly, it should be noted that there are other variables that can affect the reproducibility of structural brain network analyses, such as the resolution of the MR data, the parcellation scheme used, the time interval between the test and retest scans, and others. These variables are also worth considering in structural brain network studies, and a detailed discussion on the subject is provided in the work by Welton et al. (2015), but lies outside the scope of this manuscript.

5. Conclusions

In this study, we presented and compared several alternative graph construction schemes for structural brain networks. Our comprehensive analysis showed that the schemes exhibit different reproducibility, both for the graphs themselves and the graph-theoretical metrics. Our results indicate that employing different schemes will result in a different number of participants needed to see an effect. In order for studies to achieve the maximum power in detecting such effects, similar analysis need to always be performed at the outset.

Declarations of interest

None.

Data and code availability

The HCP test-retest data is freely available as listed above. The code used to generate the graphs for the structural brain networks with the OMST schemes is available at: https://github.com/stdimitr/multi-group-analysis-OMST-GDD. The code used to perform the reproducibility analysis is not freely available, but is based exclusively on Matlab functions. This adheres to the data and code requirements of our funders.
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