Network analysis of the worldwide footballer transfer market

MING-XIA LI\textsuperscript{1,2}, WEI-XING ZHOU\textsuperscript{2,3,4} (a) and H. EUGENE STANLEY\textsuperscript{5}

\textsuperscript{1}Research Institute of Sports Economics, East China University of Science and Technology, Shanghai 200237, China
\textsuperscript{2}Research Center for Econophysics, East China University of Science and Technology, Shanghai 200237, China
\textsuperscript{3}Department of Finance, East China University of Science and Technology, Shanghai 200237, China
\textsuperscript{4}Department of Mathematics, East China University of Science and Technology, Shanghai 200237, China
\textsuperscript{5}Center for Polymer Studies and Department of Physics, Boston University, Boston, Massachusetts 02215, USA

PACS 89.20.-a – Interdisciplinary applications of physics
PACS 01.80.+b – Physics of games and sports
PACS 89.75.Da – Systems obeying scaling laws

Abstract – The transfer of football players is an important part in football games. Most studies on the transfer of football players focus on the transfer system and transfer fees but not on the transfer behavior itself. Based on the 470,792 transfer records from 1990 to 2016 among 23,605 football clubs in 206 countries and regions, we construct a directed footballer transfer network (FTN), where the nodes are the football clubs and the links correspond to the footballer transfers. A systemic analysis is conducted on the topological properties of the FTN. We find that the in-degrees, out-degrees, in-strengths and out-strengths of nodes follow bimodal distributions (a power law with exponential decay), while the distribution of link weights has a power-law tail. We further figure out the correlations between node degrees, node strengths and link weights. We also investigate the general characteristics of different measures of network centrality. Our network analysis of the global footballer transfer market sheds new lights into the investigation of the characteristics of transfer activities.

Introduction. – Football matches are widely regarded as the most influential sport in the world. According to a survey of FIFA in 2006, 4% of the world’s population are actively involved in football. The transfer of football players became part of the football game after 1893. Up till now, the transfer records were updated again and again, and the news of footballer transfers was listed on the headlines of sports news numerous times. The active football market needs to be constantly stirred, and the continually sensational transfer is one of the driving forces.

From the birth of the world’s first million transfer to the free transfer of European football, the beautiful sport has become a booming industry. However, research on the transfer of football players focuses mostly on the transfer system and transfer fees and there is less research on the transfer behavior itself. It is found that the transfer fee is different in various segments in English professional football sports \cite{1}, and the determination of transfer fee is similar in both professional and nonleague football sports \cite{2}. Usually football players benefit from the transfer system \cite{3}; However the transfer system might also obstruct the free movement of football players between Member States in Europe and may restrict the ability of most clubs to compete for elite players \cite{4}. It is also found that in the English Football League there is no racial difference in footballers’ transfer prices \cite{5}.

In the era of big data, social science researchers consider social network analysis as an important tool to understand and excavate empirical laws of social behavior \cite{6,7}. With the rapid development of information transmission and storage technology, lots of human daily activities have been recorded. In the face of massive log data of human behavior, computational social science has attracted wide attention of researchers in recent years \cite{8,9}. Barabási points out that the ideas and methods of complex networks in the process of understanding complex social phenomena will be indispensable tools. The network links between the two bodies follow different dynamic laws during the construction process, such as assortative, correlation, and
proximity \cite{12,13}.

In recent years, network analysis has been applied to study different networks constructed from variant attributes of the football market, such as the bipartite network of players and clubs \cite{14}, football passing networks among players \cite{15,19}, zone-specified passing networks \cite{20-23}, directed footballer transfer networks (FTNs) \cite{24}, and mutual footballer transfer networks (MFTNs) \cite{25}.

In this Letter, we construct a direct transfer network to investigate the features of the transfer events of football players between different football club. Other than the study of Liu et al. \cite{24}, we mainly focus on the topological properties of the FTN.

**The footballer transfer network.** – The football player transfer records from 1990 to 2016 were retrieved from \url{http://www.transfermarkt.com}. There are 470,792 transfers among 23,765 worldwide football clubs.

We construct a footballer transfer network (FTN), in which the nodes refer to the clubs and a directed link $i \rightarrow j$ forms when a player is transferred from club $i$ to club $j$. The FTN is composed of 23,765 nodes and 243,770 directed links. It is possible that there are multiple transfers from one club to another club. In this case, only one directed link is drawn and its weight is the number of transfers. In contrast, the FTN analyzed by Liu et al. contains 410 nodes and 6316 directed links and the time period is from 2011 to 2015 \cite{24}.

There are 39 connected components or sub-networks in the FTN. The largest component contains 23,669 nodes (99.6\% of all nodes). Each smaller component has no more than 11 nodes. The components are dominated by trees and the largest network is very sparse. Hence the density of the whole network is very small (close to 0.0004) and the average clustering coefficient is not large (about 0.20). A sample FTN constructed from about 4000 transfer records on 1 January 2007 is illustrated in fig. \[1\].

**Results.** –

**Distributions.** In the FTN, a club’s out-degree $k_{\text{out}}^i$ is the number of clubs that received its football players, and a club’s in-degree $k_{\text{in}}^i$ is the number of clubs which transferred football players to it. We find that the average node degrees, $\langle k_{\text{out}} \rangle$ and $\langle k_{\text{in}} \rangle$, are close to 10.26. The maximum out-degree and in-degree are respectively $k_{\text{out}}^{\text{max}} = 235$ and $k_{\text{in}}^{\text{max}} = 177$, corresponding to the same football club, “Parma (Italy)”, which currently competes in Series A.

We find that there are no nodes with $k_{\text{in}} = 0$ and $k_{\text{out}} = 0$, meaning that no club is isolated from other clubs in the transfer market. The number of nodes with $k_{\text{in}} = 0$ and $k_{\text{out}} > 0$ is 4746. These nodes usually correspond to football training clubs. For example, club “Yonsei Univ (Korea, South)”, a squad of Yonsei University, has and in-degree of 0 and an out-degree of 24. A rookie football player goes to these clubs for training because professional clubs do not welcome inexperienced players. They need to improve their skills and show their abilities on football pitches. The number of nodes with $k_{\text{in}} > 0$ and $k_{\text{out}} = 0$ is 1779. These nodes most probably correspond to professional football clubs. For example, club “Reno FC (United States)”, a second tier in United Soccer League, has an in-degree of 18 and an out-degree of 0. These clubs may have good rankings and provide good salaries. Most football players want to enter those clubs and will scarcely transfer out.

In the FTN, the weight $w_{ij}$ of a directed link $i \rightarrow j$ represents the number of football players transferred from club $i$ to club $j$. The average weight of all the links in the FTN is $\langle w \rangle = 1.67$, indicating the average number of football players transferred from one club to another is less than 2. It implies that most football clubs have transferred only one football player. The link with the maximum weight connects two football clubs, “Akademia FCSM (Russia)” and “Spartak Moskow II (Russia)”. The reason is that the former club is the academy of the next one.

The in-strength and out-strength of a node $i$ can be
is to investigate the average neighbor node degree:

\[ k_{nn,i} = \frac{1}{k_i} \sum_{j \in \mathcal{N}_i} k_j, \]

where \( \mathcal{N}_i \) is the set of nearest neighbor nodes of \( i \) which are directly connected to node \( i \). By averaging \( k_{nn} \) over all the nodes with degree \( k \), we can observe the correlation between \( k_{nn} \) and \( k \), as shown in fig. 3(a). Since a node has an out-degree and an in-degree, we obtain four correlations between node degree \( k \) and average neighbor node degree \( k_{nn} \). All the four lines have an increasing trend with the increase of node degree. It indicates that the FTN exhibits an assortative mixing pattern, just like many other social networks \[29,34–36\]. The direction of links in the FTN do not have great impact on this feature \[25\].

### Correlations

In social networks, an interesting result is that nodes with similar characteristics will prefer to connect with each other, called assortative mixing \[29\]. In some case of social networks, it is also known as the homophily \[30–33\]. One way to detect such feature in FTN is to investigate the average neighbor node degree:

\[ k_{nn,i} = \frac{1}{k_i} \sum_{j \in \mathcal{N}_i} k_j, \]

where \( \mathcal{N}_i \) is the set of nearest neighbor nodes of \( i \) which are directly connected to node \( i \). By averaging \( k_{nn} \) over all the nodes with degree \( k \), we can observe the correlation between \( k_{nn} \) and \( k \), as shown in fig. 3(a). Since a node has an out-degree and an in-degree, we obtain four correlations between node degree \( k \) and average neighbor node degree \( k_{nn} \). All the four lines have an increasing trend with the increase of node degree. It indicates that the FTN exhibits an assortative mixing pattern, just like many other social networks \[29,34–36\]. The direction of links in the FTN do not have great impact on this feature \[25\]. Besides that, each curve can be approximated by two power laws.

The average neighbor edge weight \( w_{ne,ij} \) of link \( i \to j \) for the MFTN has been studied \[25\]. We can calculate \( w_{ne,ij} \) for the FTN similarly. We create a new undirected subordinate network FTN*, where the nodes are mapped from the links in the FTN and a link is created if two links \( i \to j \) (or \( j \to i \)) and \( i \to k \) in the FTN have a common node \( i \).

For simplicity, we do not consider the bi-directed links as a pair of neighbor links, that is, we require that \( j \neq k \). Thus, the neighbors of a link in the FTN is converted to the
neighbors of a node in the FTN*. The average neighbor link weight \( w_{ne,ij} \) of a link is calculated as follows:

\[
\begin{align*}
  w_{ne,ij} &= \sum_{a \neq i, j} \left( w_{aj} + w_{ib} + w_{ja} + w_{lb} \right) \\
  &= \frac{s_i^{\text{out}} + s_j^{\text{in}} + s_j^{\text{out}} + s_i^{\text{in}} - 2w_{ij} - 2w_{ji}}{k_i^{\text{out}} + k_i^{\text{in}} + k_j^{\text{out}} + k_j^{\text{in}} - 4}.
\end{align*}
\]

The average neighbor link weight \( \langle w_{ne} | w \rangle \) for the edges of weight \( w \) is calculated by averaging \( w_{ne,ij} \) over those edges of weight \( w \). Fig. 3(b) shows the average neighbor link weight \( \langle w_{ne} | w \rangle \) as a function of weight \( w \). \( \langle w_{ne} | w \rangle \) moves within [1,7,2] when \( w < 30 \). When \( w > 30 \), the fluctuation of \( \langle w_{ne} | w \rangle \) become drastic. It indicates that the number \( w \) of transfers between two clubs in the FTN distributes more randomly than the number of clubs that a club transferred with \( k \).

The average nearest neighbor strength \( s_{nn} \) of node \( i \) is the average strength of \( i \)'s nearest neighbors:

\[
  s_{nn,i} = \frac{1}{k_i} \sum_{j \in N_i} s_j.
\]

Like the similarity between the distributions of node degrees and node strengths (see fig. 2), the correlation between \( s_{nn} \) and \( s \) is quite similar to the correlation between \( k_{nn} \) and \( k \).

Since the distributions of node degrees and node strengths are similar to each other, one may expect that the average node strength has a linear correlation with the node degree \( k \):

\[
  \langle s | k \rangle \sim k^{\alpha_{ss_1}}
\]

with \( \alpha_{ss_1} = 1 \), if there is no correlation between the node degree and the weights of the edges linked to the node. We also check the correlation between the product of node strength and node degree,

\[
  \langle s_i s_j | k_i k_j \rangle \sim (k_i k_j)^{\alpha_{ss_2}}
\]

where nodes \( i \) and \( j \) belong to link \( i \rightarrow j \).

Fig. 4 shows the correlations between node degrees and node strengths. Very nice power-law dependence is observed. The power-law exponents are estimated as follows: \( \alpha_{ss_1} \text{(out)} = 1.06, \alpha_{ss_1} \text{(in)} = 1.10 \) in fig. 4(a) and
\[ \alpha_{ks1}(\text{out,out}) = 1.08, \alpha_{ks1}(\text{out,in}) = 1.09, \alpha_{ks1}(\text{in,out}) = 1.10, \alpha_{ks1}(\text{in,in}) = 1.07 \text{ in fig. 4(b)}. \] All the values of \( \alpha_{ks1} \) and \( \alpha_{ks2} \) are greater than 1, which are close to the case of MFTN [20].

As the correlation exists between node degrees and link weights, we study the variation curve between link weights with respect to node degree \( k \) and node strength \( s \). (a) The average link weight \( \langle w_{ij} \rangle |k, k'\rangle \) of the directed links from \( i \) to \( j \) whose degrees are \( k_i \) and \( k_j \). (b) The average link weight \( \langle w_{ij} \rangle |s, s'\rangle \) of the directed links from \( i \) to \( j \) whose strengths are \( s_i \) and \( s_j \).

Network Centrality. Network centrality is a measure of how central a node locates in the network. Obviously, node degree is one of the centrality measures. Besides that, we also investigate other two commonly used centrality measures, betweenness centrality and closeness centrality. Betweenness centrality characterizes the importance of a node in network flow [39,40]:

\[ b_j = \sum_{i \neq j \neq k} \frac{\sigma_{ik}(j)}{\sigma_{ik}}, \]

where \( \sigma_{ik} \) is the number of shortest paths from node \( i \) to node \( k \) and \( \sigma_{ik}(j) \) is the number of those paths that pass through node \( j \). By dividing the number of pairs of nodes that do not contain node \( j \), we can obtain the normalized betweenness centrality \( b^n_j = b_j/[(N-1)(N-2)] \). If \( b^n_j \) is close to 1, all paths in the network will pass through node \( j \). In a connected network, a node’s closeness is the average shortest path length between this node and other nodes [41]. Since the FTN is not fully connected, we use the Harmonic centrality instead [42]:

\[ H^\text{out}(i) = \sum_{i \neq j} \frac{1}{d(i,j)}, H^\text{in}(i) = \sum_{i \neq j} \frac{1}{d(j,i)}, \]

where \( d(i,j) \) is the shortest path length from node \( i \) to node \( j \). By dividing \( N - 1 \), we get the normalized Harmonic centrality \( H^n = H/((N - 1)) \). The larger \( H^n_i \) is, the closer node \( i \) is to other nodes. If \( H^n_i = 0 \), node \( i \) is disconnected with all of the other nodes, which means node \( i \) is the isolated node. If \( H^n_i = 1 \), node \( i \) is directly linked with all the other nodes. The graph is a star-like network and node \( i \) is the center of the network.

Fig. 5 shows the distributions of betweenness centrality and closeness centrality of the nodes in the FTN. One can observe that with the increase of \( b^n \), the probability \( p \) becomes smaller. The average normalized betweenness centrality \( \langle b^n \rangle \) is close to 0.00011. It implies that most football clubs do not play an important role in the football players transfer market. The football club with the largest betweenness centrality \( b^n_{\text{max}} = 0.0063 \) (about 600 times the average) is “Parma (Italy)”, which is not surprising as “Parma (Italy)” has the largest in-degree and out-degree. The distribution shape of the closeness centrality in fig. 5(b) is quite different from the betweenness centrality. One can find a peak presents in both curves. The peak locates at \( H^n \approx 0.16 \) for the closeness centrality from outgoing links and \( H^n \approx 0.20 \) for the closeness centrality from incoming links. And the distribution of \( H^n,\text{out} \) is on the left side of the distribution of \( H^n,\text{in} \). Considering the nodes with large closeness, we find that the closeness from outgoing links is smaller than the closeness from incoming links on average. Moreover, the number of nodes with small closeness \( H^n < 0.001 \) from incoming links is larger than that from outgoing links. It indicates that many leaf nodes only have outgoing links, corresponding to football training clubs.

In social network analysis, the centralization of a network is a measure of how equal the centralities of the nodes are in the network [43], which is calculated as the differences between the centralities of the most central node and all other nodes. For a directed network, one considers centralization as the difference between the out-directional.
we calculate the strength centralization $C_s = C_{s}^{\text{in}} - C_{s}^{\text{out}}$, where $\max \sum_{i=1}^{N}(s_i^{\text{max}} - s_i^y) = (N - 1)\sum_{i=1}^{N} s_i^y$. The weighted network centralization $C_s$ has the same physical meaning as the unweighted network centralization $C_k$.

In the FTN, the degree centralizations are $C_{k}^{\text{in}} = 0.0070$, $C_{k}^{\text{out}} = 0.0095$, $C_k = -0.0024$, and the strength centralizations are $C_{s}^{\text{in}} = 0.0009$, $C_{s}^{\text{out}} = 0.0017$, $C_s = -0.0008$. All the centralizations are close to 0. It implies that no extreme dominating club exists in the global football player transfer market.

If we use $b^n$ for $x$ in Eq. (11), we obtain the betweenness centralization $C_b$, where $\max \sum_{i=1}^{N}(b_i^{n_{\text{max}}} - b_i^n) = N - 1$. When $C_b$ is close to 1, some football clubs in the network act as the transfer center. Otherwise, there is no transfer center in the network. We obtain that $C_b = 0.0062$ for the FTN. If we replace $x$ in Eq. (11) with $H^n$, we obtain the closeness centralization $C_H$, where $\max \sum_{i=1}^{N}(H_i^{n_{\text{max}};y} - H_i^{n;y}) = N - 1$. For the FTN, we have $C_{H}^{\text{out}} = 0.1027$, $C_{H}^{\text{in}} = 0.1412$ and $C_H = 0.0385$. We find the closeness centralization from outgoing links is smaller than that from incoming links, which is different from the website network.

**Summary and discussions.** — In this letter, we constructed a directed football player transfer network by using more than 470,000 transfer records of football players around the world from 1990 to 2016. We investigate the topological characteristics of the network.

We first investigated the distributions of in-degrees and out-degrees of node, link weights, and in- and out-strengths of nodes. We found that the distributions of node degrees and node strengths can be fitted to bimodal distributions [26], which might result from the different transfer paths of football players from different football clubs. We also found that the link weight distribution has a power-law tail. We further inspected the correlations among node degrees, node strengths and link weights. It is found that the neighbor node degree (strength) increases with the increase of node degree (strength), indicating the FTN is assortative mixing. We also found that link weights correlate with node degrees, which is similar to the results in mobile phone communication network [36]. These properties have been studied for the mutual footballer transfer network [25]. The corresponding properties for the FTN and MFTN are qualitatively similar, but they exhibit quantitative differences.

By analyzing various network centrality measures, we unveiled that most nodes have a small centrality, suggesting that no club acted as a transfer center. Investigation of the difference between the centralities of the most central node and all other nodes shows that all the football clubs occupy similar positions in the transfer network, and the closeness centralization from outgoing links is smaller than that from incoming links. It suggests that further studies on the FTN at meso-scales or micro-scales are required to uncover the different roles the clubs may play in the global transfer market.
REFERENCES

[1] Dobson S. and Gerrard B., J. Sport Manage., 13 (1999) 259.
[2] Dobson S., Gerrard B. and Howe S., Appl. Econ., 32 (2000) 1145.
[3] Dietl H. M., Franck E. and Lang M., Eur. J. Law Econ., 26 (2008) 129.
[4] Pearson G., Eur. Law J., 21 (2015) 220.
[5] McDonald J., Appl. Econ. Lett., 15 (2008) 865.
[6] Barabási A.-L., Nature, 435 (2005) 207.
[7] Jiang Z.-Q., Xie W.-J., Li M.-X., Podobnik B., Zhou W.-X. and Stanley H. E., Proc. Natl. Acad. Sci. U.S.A., 110 (2013) 1600.
[8] González M. C., Hidalgo C. A. and Barabási A.-L., Nature, 453 (2008) 779.
[9] Wasserman S. and Faust K., Social network analysis: Methods and applications (Cambridge university press, Cambridge) 1994.
[10] Squartini T., Lelyveld I. and Garlaschelli D., Sci. Rep., 3 (2013) 3357.
[11] Bargigli L., de Iasio G., Infante L., Lillo F. and Pierobon F., Quant. Financ., 3 (2013) 3357.
[12] Li M.-X., Palchykov V., Jiang Z.-Q., Kaski K., Kertész J., Micciché S., Tummino M., Zhou W.-X. and Mantegna R. N., New J. Phys., 16 (2014) 083038.
[13] Jiang Z.-Q. and Zhou W.-X., Physica A, 389 (2010) 4929.
[14] Onody R. N. and de Castro P. A., Phys. Rev. E, 70 (2004) 037103.
[15] Yamamoto Y. and Yokoyama K., PLoS One, 6 (2011) e29638.
[16] Clemente F. M., Martins F. M. L., Kalamaras D., Wong D. P. and Mendes R. S., Int. J. Perform. Anal. Sport., 15 (2015) 80.
[17] Clemente F. M., Martins F. M. L., Wong D. P., Kalamaras D. and Mendes R. S., Int. J. Perform. Anal. Sport., 15 (2015) 704722.
[18] McLean S., Salmon P. M., Gorman A. D., Stevens N. J. and Solomon C., Hum. Mov. Sci., 57 (2018) 400.
[19] Mendes B., Clemente F. M. and Maurício, J. Hum. Kinet., 61 (2018) 141.
[20] Cotta C., Mora A. M., Merelo J. J. and Merelo-Molina C., J. Syst. Sci. Complex., 26 (2013) 21.
[21] Narizuka T., Yamamoto K. and Yamazaki Y., Physica A, 412 (2014) 157.
[22] Clemente F. M., Martins F. M. L., Wong D. P., Kalamaras D. and Mendes R. S., Kinesiology, 48 (2016) 103.
[23] Clemente F. M., Jose F., Oliveira N., Martins F. M. L., Mendes R. S., Figueiredo A. J., Wong D. P. and Kalamaras D., J. Hum. Sport Exerc., 11 (2016) 376.
[24] Liu X. F., Liu X.-H., Wang Q.-X. and Wang T.-X., PloS ONE, 11 (2016) e0156504.
[25] Li M.-X., Xiao Q.-L., Wang Y. and Zhou W.-X., Int. J. Mod. Phys. B, 33 (2018) in press.
[26] Wu Y., Zhou C.-S., Xiao J.-H., Kurths J. and Schellnhuber H. J., Proc. Natl. Acad. Sci. U.S.A., 107 (2010) 18803.
[27] Barabási A.-L. and Albert R., Science, 286 (1999) 509.
[28] Clauset A., Shalizi C. R. and Newman M. E. J., SIAM Rev., 51 (2009) 661.
[29] Newman M. E. J., Phys. Rev. Lett., 89 (2002) 208701.
[30] McPherson M., Smith-Lovin L. and Cook J. M., Annu. Rev. Sociol., 27 (2001) 415.
[31] Currarini S., Jackson M. O. and Pin P., Econometrica, 77 (2009) 1003.
[32] Kovanen L., Kaski K., Kertész J. and Saramäki J., Proc. Natl. Acad. Sci. U.S.A., 110 (2013) 18070.
[33] Kossinets G. and Watts D. J., Amer. J. Sociol., 115 (2009) 405.
[34] Catanzaro M., Caldarelli G. and Pietronero L., Phys. Rev. E, 70 (2004) 037101.
[35] Rivero M. T., Soderstrom S. B. and Uzzi B., Annu. Rev. Sociol., 36 (2010) 91.
[36] Li M.-X., Jiang Z.-Q., Xie W.-J., Micciché S., Tummino M., Zhou W.-X. and Mantegna R. N., Sci. Rep., 4 (2014) 5132.
[37] Barrat A., Barthélémy M., Pastor-Satorras R. and Vespignani A., Proc. Natl. Acad. Sci. U.S.A., 101 (2004) 3747.
[38] Onnela J.-P., Saramäki J., Hyvönen J., Szabó G., de Menezes M. A., Kaski K., Barabási A.-L. and Kertész J., New J. Phys., 9 (2009) 179.
[39] Freeman L. C., Socio. Networks, 40 (1977) 35.
[40] Brandes U., J. Math. Soc., 25 (2001) 163.
[41] Bavelas A., J. Acoust. Soc. Amer., 22 (1950) 752.
[42] Marchiori M. and Latora V., Physica A, 285 (2000) 539.
[43] Freeman L. C., Soc. Networks, 1 (1979) 215.
[44] Li M.-X., Jiang Z.-Q., Xie W.-J., Xiong X., Zhang W. and Zhou W.-X., Physica A, 419 (2015) 575.
[45] Adamic L., Brunetti C., Harris J. and Kirilenko A. A., Econometrica, 20 (2017) 8126.