Phonon-Related Monochromatic THz Radiation and its Magneto-Modulation in 2D Ferromagnetic Cr₂Ge₂Te₆

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Searching multiple types of terahertz (THz) irradiation source is crucial for the THz technology. In addition to the conventional fermionic cases, bosonic quasi-particles also promise energy-efficient THz wave emission. Here, by utilizing a 2D ferromagnetic Cr₂Ge₂Te₆ crystal, first a phonon-related magneto-tunable monochromatic THz irradiation source is demonstrated. With a low-photonic-energy broadband THz pump, a strong THz irradiation with frequency \(\approx 0.9\) THz and bandwidth \(\approx 0.25\) THz can be generated and its conversion efficiency could even reach 2.1% at 160 K. Moreover, it is intriguing to find that such monochromatic THz irradiation can be efficiently modulated by external magnetic field below 160 K. According to both experimental and theoretical analyses, the emergent THz irradiation is identified as the emission from the phonon-polariton and its temperature and magnetic field dependent behaviors confirm the large spin-lattice coupling in this 2D ferromagnetic crystal. These observations provide a new route for the creation of tunable monochromatic THz source which may have great practical interests in future applications in photonic and spintronic devices.

1. Introduction

Terahertz (THz) radiation source plays a crucial role in relevant research and applications. After decades of intensive cultivation, the playground of THz sources have been widely developed in many materials, such as semiconductors,[1] nonlinear electro-optic crystals,[2] surface plasma,[3] metamaterials,[4] ferro-/non-magnetic heterojunctions,[5] etc. Recently, with extraordinary electrical and optical properties, 2D van der Waals (vdWs) materials have been also used for the novel THz irradiation source development.[6] For instance, Huang et al. reported the THz surface emission based on the competition between surface optical rectification and photocurrent surge in layered MoS₂.[7] Under the excitation of strong infrared pulses, Suo et al. proposed a new THz emitter based on the shift current occurring on the inversion-broken surface of layered CrSiTe₃ crystal.[8] With
the aid of laser-excited surface plasmon on a gold substrate, Balh et al. observed an enhanced THz emission from the single-layered graphene.\(^{[3]}\) In the majority of these studies, THz radiation based on 2D vdWs materials is originating from photocative field,\(^{[4]}\) optical rectification, and laser-induced plasma, which all belong to the fermion (electron) catalog and generally bring broadband THz emission with low conversion efficiency.

In addition to the broadband cases, monochromatic THz sources are also important and it possesses immense potential in practical applications,\(^{[10]}\) especially in communication technology.\(^{[11]}\) According to the protocol of the International Telecommunication Union (ITU), the better monochromaticity of the waves in communication usually means higher band utilization and lower interference risk.\(^{[12]}\) From visible light to near-infrared band, the monochromatic radiation sources (MRS) are usually realized by exciting the electronic transition between the direct bandgap of specific semiconductors.\(^{[13]}\) While to the extent of MRS in mid- and far-infrared range, the radiation sources would extend from fermionic particles to bosonic cases, such as phonons.\(^{[14]}\)

For THz wave with lower photon energy, its MRS would extend from fermionic particles to bosonic cases, such as phonons.

\[ \text{frequency} \approx \text{radiation} \]

It was found that a strong THz irradiation with frequency \(\approx 0.9 \text{ THz} \) and bandwidth \(\approx 0.25 \text{ THz} \) can be generated with a low-photonic-energy broadband THz pump. The conversion efficiency varies with temperature and can even reach 2.1% at 160 K. This could be attributed to the competition between attenuated absorption caused by semiconductor property and enhanced absorption due to the ferromagnetism during the cooling process (see more detail in Part I and Figure S1, Supporting Information).\(^{[15]}\) Apart from the main wave, it is intriguing to find that there are additional oscillations superimposed on the rear portion of the main waveforms (black arrow in Figure 1b). Such THz oscillations emerge at 225 K and exist until the lowest temperature of 10 K we measured. Its amplitude slightly varies with temperature and reaches the maximum at 120 K.

There are two possible origins for these additional oscillations. One is Fabry–Pérot effect that arises from multiple reflections between internal interfaces of the sample, another is electromagnetic (EM) radiations. The loss functions for both experimental results and theoretical predictions of Fabry–Pérot effect were calculated.\(^{[16]}\) As shown in the Figure S2 (Supporting Information), the experimental result is significantly different from the theoretical feature of the Fabry–Pérot effect. Especially, the loss function of these oscillations corresponds to the THz response around 0.9 THz and could even be negative, which indicates negative loss after penetrating the sample. In order to further explore the additional oscillations, the fast-Fourier-transformation from TDS results was done and the corresponding typical frequency domain spectra (FDS) results are depicted in Figure 1c. By comparing the results of 300 K (red curve) and 120 K (blue curve), it is found that the additional oscillations yield a certain frequency of around 0.9 THz. Especially, at 120 K, the amplitude of output THz wave at \(\approx 0.9 \text{ THz} \) is almost 2.7 times of the 300 K case and even higher than the free-space pinhole reference (black curve), as shown in the inset of Figure 1c.

### 2. Results and Discussions

To create a phonon-based THz emitter, appropriate materials are important. In addition to intensively studied metamaterial and graphene, 2D vdWs magnetic materials are another ideal material for this purpose because their exotic properties and their strong spin-phonon coupling are expected to give effective responses to external magnetic fields.\(^{[17]}\) Cr\(_2\)Ge\(_2\)Te\(_6\) is one of the prototypes. It undergoes a paramagnetic-ferromagnetic transition at \(T_c = 68 \text{ K} \).\(^{[18]}\) The THz transmission response of Cr\(_2\)Ge\(_2\)Te\(_6\) single crystal was measured by means of a home-built terahertz time domain spectroscopy system (THz-TDS) system as schematically shown in Figure 1a. The measurements were taken from room temperature to 10 K with an Oxford SpectroMag He-bath cryostat (see details in Experimental Section). After penetrating through the sample, the time-resolved THz signals were collected and the typical results are depicted in Figure 1b. In the time domains of transmitted THz wave obtained at 300 K, there is a main wave that has the same shape as the incident THz wave with lower intensity due to the absorption of Cr\(_2\)Ge\(_2\)Te\(_6\) crystal. With the temperature decreasing, the intensity of the main wave increases at first and then drops below 160 K. This could be attributed to the competition between attenuated absorption caused by semiconductor property and enhanced absorption due to the ferromagnetism during the cooling process (see more detail in Part I and Figure S1, Supporting Information).\(^{[19]}\) Apart from the main wave, it is intriguing to find that there are additional oscillations superimposed on the rear portion of the main waveforms (black arrow in Figure 1b).

Surprisingly, little attention has been devoted to the study of 2D vdWs bosonic THz wave and no cogenetic phonon-based monochromatic THz radiation has been published yet. Here, by choosing ferromagnet Cr\(_2\)Ge\(_2\)Te\(_6\) as a model system, we firstly demonstrate a 2D phonon-based monochromatic THz radiation. It was found that a strong THz irradiation with frequency \(\approx 0.9 \text{ THz} \) and bandwidth \(\approx 0.25 \text{ THz} \) can be generated with a low-photonic-energy broadband THz pump. The conversion efficiency varies with temperature and can even reach 2.1% at 160 K. Moreover, it is intriguing to find that the external magnetic field \(B\) could efficiently modulate such monochromatic THz irradiation especially when \(B\) is parallel to the \(ab\)-plane of the 2D Cr\(_2\)Ge\(_2\)Te\(_6\) crystal. After carefully experimental and theoretical examining, the emergent THz irradiation is identified as the emission from the phonon-polariton in this 2D ferromagnetic crystal. Our findings suggest that the use of 2D materials may provide a variable source for bosonic-related monochromatic THz radiation.
Figure 1. Terahertz responses of Cr$_2$Ge$_2$Te$_6$ crystal. a) Schematic diagram of the transmission measurement configuration. b) Time-resolved THz spectra transmitted through the sample at some critical temperatures. c) Frequency-domain THz spectra correspond to temperatures of 300 K (red curve) and 120 K (blue curve). The black curve is the reference THz signal through the pinhole of the sample holder without any sample. The inset is the close-up view of the red dashed frame area at 120 K.

loss function and large output THz wave at $\approx 0.9$ THz, it is reasonable to conclude that the additional oscillations are emergent THz radiation.

Furthermore, by calculating the FDS of transmittance variation ($\Delta T$) of specific temperature with reference to 300 K that without radiation emerged (Figure S3, Supporting Information), it is found that the additional oscillation is monochromatic and its center frequency, monochromaticity, and amplitude are strongly dependent on temperature. Figure 2a presents the temperature dependence of the center frequency ($f_c$) and full-width at half-maximum (FWHM) of the THz radiation. At first glance, the most important common performance is that the temperature dependence of $f_c$ and FWHM separate the temperature coordinate into three regions with boundaries of 160 K and $T_C$. While the striking contrast is that their dependencies are opposite. Specifically, for the case of $f_c$, when the temperature drops from 220 to 160 K, it first dramatically increases from 0.80 to 0.87 THz. While in the following region from 160 K to $T_C$, it turns to increase in a slowing trend from 0.87 to 0.90 THz. Afterward, at temperatures lower than $T_C$, the frequency is further hardened to 0.93 THz. However, for the FWHM that indicates the monochromaticity of the radiations, its temperature dependence in these three regions corresponds to the narrowing from 0.46 to 0.35 THz rapidly (220 to 160 K), the approximate plateau form from 0.35 to 0.32 THz (160 K to $T_C$), and a further narrowing to 0.25 THz below $T_C$, respectively.

As a rule of thumb, the conversion efficiency ($\psi$) is a critical characteristic.[27] Here, the radiation performance is evaluated with the parameter of $\psi = I_r/I_{ab} = E_o^2/(E_i^2 - E_t^2)$, where $I_{ab}$ and $I_r$ are power (intensity) of absorbed pump pulse and generated THz radiation, in which the THz power is proportional to the square of its field amplitude. $E_o$ is the P-P amplitude of the first oscillation waveforms, $E_i$ and $E_t$ are P-P amplitude of the incident and transmitted THz waveforms, respectively. Corresponding results are shown as hexagonal symbols in Figure 2b. The $\psi$ also shows the same temperature regions as $f_c$ and FWHM. From 220 to 160 K, the $\psi$ starts to emerge and first be dramatically enhanced to $\approx 2.1\%$, which is higher than the cases of fermionic cases, such as photoconductive and nonlinear optical rectification (usually lower than 0.1%).[28] Whereas in the region below 160 K, the increasing trend then gradually transforms into a declining one. Peculiarly, for temperatures below $T_C$, it is dramat-
above the spin fluctuation temperature (the temperature dependence of \(T_s \approx 160 \text{ K} \)) and the THz radiation frequency (originating from the formation of magnetic correlations.\(^{[25a,b,29]}\))

Two critical temperatures (160 K and \(T_c \approx 0.9 \text{ THz/3.7 meV} \)) of \(\text{Cr}_2\text{Ge}_2\text{Te}_6\) could attribute to the enhanced THz absorption of the sample was cooling from room temperature down to 25 K. As shown by its first-order derivative curve in the inset of Figure 2b, the critical temperatures corresponding to the decreasing slope variations are 160 K and \(T_c \approx 0.9 \text{ THz/3.7 meV} \) at \(T = 160 \text{ K} \), which are same as those for the parameters of the THz emission. Such coincidence implies that the observed THz emission is associated with the inter-layered phonons in this 2D vdW's ferromagnetic material.

Owing to the unit cell of the \(\text{Cr}_2\text{Ge}_2\text{Te}_6\) expanded along \(c\)-axis, the Brillouin zone is folded in the momentum space, resulting in the emergence of zone-folded phonon modes. Based on the XRD results, we calculated the phonon dispersion of the expanded hexagonal cell (see detailed results in Figure S4, Supporting Information). As notably shown with red arrows in the inset of Figure 3a, there is an inter-layered longitudinal vibration mode, corresponding to a non-centrosymmetric longitudinal optical (LO) layer-breathing mode with frequency (\(\omega_{\text{LO}} \)) of \(\approx 0.92 \text{ THz} \) at \(\Gamma \) point. Such LO mode with the three layers within each unit cell possesses different vibration amplitudes (red curve in Figure 3a). It should be emphasized that this LO layer-breathing mode, which breaks the inversion center and degenerates the space group from \(R\overline{3}m\) to \(R3\), is dipole active and gives rise to piezoelectricity.\(^{[13]}\) Interestingly, due to the piezoelectricity and generalized Hooke’s law of the updated group, some co-frequency transverse vibrations with transversal polarization (TP) can be driven by the vibration of LO phonons, as schematically shown with the (1) of Figure 3b. According to the Lyddane-Sachs-Teller (LST) relation,\(^{[16]}\) after pumping by a THz pulse envelope with transversal polarized electric field, the incident EM waves with frequency close to the LO layer-breathing mode could effectively propagate in \(\text{Cr}_2\text{Ge}_2\text{Te}_6\) and strongly coupled with the co-frequency TP and form a new bosonic quasi-particle, i.e., so-called phonon-polariton (P-Polariton).\(^{[34]}\) After that, these photon pumping induced bosonic P-Polariton could in turn generate far-field EM radiation with frequency close to the original LO phonon as schematically illustrated by process (2) and (3) in Figure 3b.\(^{[14c,35]}\) While for the transverse optical (TO) phonon mode, there exist certain absorption and reflection loss during the propagating process. The TO mode also happens to be at the peak of the frequency spectrum of the THz system. There is neither distinct loss effect nor TO phonon involved radiation effect observed. Moreover, due to the energy of this bosonic P-Polariton generated THz radiation is carried in the piezoelectricity vibration, it is reasonable to consider it as a highly efficient bosonic laser-like process.\(^{[12,36]}\) Beyond that, according to the further calculations (Figure S5, Supporting Information), it was found that the \(c\) constant dependent evolution of phonon frequency is consistent with both the experimental results of \(\omega_{\text{LO}} \) shown in Figure 2a and the previous reports of interactions between spin and dipole-active phonon mode in 2D magnets.\(^{[21,37]}\)

According to the above discussion and the tensor symmetry of \(R3\) structure, it can be predicted that, for a certain THz-Pump field, the electric displacement and corresponding THz radiation should possess a 6-fold in-plane symmetry (see Part VI of the Supporting Information). In order to confirm this issue, the
in-plane anisotropic dependence of the THz radiation amplitude was investigated by tuning the in-plane azimuth of the sample. As shown in Figure S6b (Supporting Information), it exhibits a cycle of $\pi/3$ that matches well with the 6-fold symmetry of the P-Polariton as predicted. In addition, the THz excitation amplitude dependence of the radiation amplitude was also investigated by inserting two THz polarizers after the low-temperature-grown GaAs photoconductive antenna (LT-GaAs-PCA). As shown in Figure S6d (Supporting Information), the radiation and excitation amplitudes are linearly correlated and there is no saturation and threshold observed, which is also good consistent with the feature of bosonic lasing reported before. These features not only indicate that the radiation effect could be further improved by enhancing the stimulation intensity, but also means that the stimulated irradiation source in Cr$_2$Ge$_2$Te$_6$ is extremely sensitive to the weak THz field ($\approx 1$ kV cm$^{-1}$). This is in good accordance with the extremely high sensitivity of Cr$_2$Ge$_2$Te$_6$ to external low-intensity photonic field. Unlike other THz sources based on 2D materials,[23,29–31] this unique THz-MRS takes full advantage of the inter-layered breathing phonons and achieves highly efficient monochromatic THz radiations with stimulation of low-energy THz pulse. This mechanism is of great practical interests, such as monochromatic THz laser, integrated gain-type monochromatic THz filter, key relay components in photonic communication, etc.

Different from other 2D semiconductors, Cr$_2$Ge$_2$Te$_6$ holds ferromagnetism. Except for electron and phonon, spin is non-negligible degree and it has been demonstrated that there exist strong spin-phonon interactions in Cr$_2$Ge$_2$Te$_6$ and its isostructural Cr$_2$Si$_2$Te$_6$ materials.[23,39] As presented in Figure 2, it is found that not only the c-axis lattice constant but also the amplitude, frequency, and FWHM of the emergent THz emission have abnormal near around the $T_c$ of Cr$_2$Ge$_2$Te$_6$ crystal, which also implies the subtle interplays between the phonon-involved THz radiation and spin orders. Hence, it is reasonable to expect that the THz radiation could also be tuned by external magnetic field ($B$).

The effect of $B$ on the THz radiations was investigated by the THz-TDS system with a superconductor magnet. The system stability under high magnetic field was verified beforehand (see Figure S7a, Supporting Information). At low temperatures, there is significant variation of the THz response that could be observed when $B$ is applied (see Figure S7b–d (Supporting Information). In order to present the magnetic field effect on the THz emission, the relative THz amplitude variation $\Delta R_B$ was defined as $\Delta R_B = \frac{(R_B - R_{B0})}{R_{B0}}$, in which $R_B$ and $R_{B0}$ are THz responses of Cr$_2$Ge$_2$Te$_6$ crystal with and without $B$ applied. The magnetic field dependence of $\Delta R_B$ obtained at corresponding $f_c$ and different temperatures were summarized in Figure 4a–f. For $B$/c-axis, the $\Delta R_B$ is negligible above $T_c$ and it is also small ($< 5\%$) below $T_c$. When $B$/ab-plane, the $\Delta R_B$ starts to emerge around 160 K and increases with decreasing of the temperature. Notably, at 10 K, the $\Delta R_B$ in ab-plane could reach the maximum of around $-20\%$ (with $B = 5$ T), which is greater than the case of c-axis ($\approx 3\%$). Such anisotropic feature of the magnetic field modulation effect on $\Delta R_B$ can be clearly observed in Figure 4g, in which the temperature-dependent $\Delta R_B$ under $B = 5$ T is plotted. By applying an external magnetic field, the spin state of the Cr$_2$Ge$_2$Te$_6$ crystal can be modified for both long-range order (below $T_c$) and short-range order ($T_c < T < 160$ K).[29,30] As one of the possible mechanisms, the magnetic field induced the spin-flips scattering could suppress the electron-phonon interactions as well as the dipole active phonon involved P-Polariton.[40] Accordingly, with such large spin-phonon coupling in this 2D ferromagnetic material, the switching of spin state by $B$ would bring the modulation of phonon-related THz emission. Moreover, the
spontaneous spin orientation of Cr$_2$Ge$_2$Te$_6$ is along c-axis. And then, from viewpoint of spin modulation, the magnetic field effect is significant when B//ab-plane. While for the case of B//c-axis, the spin orientation is not modified much under the codirectional magnetic field and the Delta $R_b$ does not seem to be perturbed as much as the B//ab-plane case. These are consistent with our observations shown in Figure 4. The magneto modulation effect provides another proof for its P-Polariton-related radiation mechanism. All these features not only offer another degree of freedom for the regulation of THz radiation in practical applications, but also provide a piece of convincing evidence for the correlation between the THz radiation, phonons, and spin orders.

3. Conclusion

In summary, benefiting from the coherent LO layer-breathing mode, a magneto-tunable monochromatic THz radiation was demonstrated in a 2D vdWs ferromagnet Cr$_2$Ge$_2$Te$_6$. After pumping by a broadband THz wave, a strong monochromatic THz irradiation can be generated. The frequency, FWHM, and the intensity of the emergent THz radiation vary with the temperature and its conversion efficiency could even reach 2.1% at 160 K. Our experimental and theoretical analyses indicate that the emergent THz irradiation is from the pump induced phonon-polariton in this 2D vdWs material. Moreover, due to the existing strong spin-phonon coupling, it is interesting to find that such monochromatic THz irradiation can be efficiently modulated by the magnetic field below 160 K. In addition to the general ferromic cases, our findings suggest that the use of 2D vdWs ferromagnet might provide a viable source for the realization of bosonic THz source with tunable and monochromatic features, which may have great practical interests in future applications in photonic and spintronic devices.

4. Experimental Section

The Cr$_2$Ge$_2$Te$_6$ single crystals are prepared with the self-flux technique, following the procedure described in ref. [41]. The effective size of the sample is $\approx 6 \times 4 \times 0.2$ mm. The terahertz data was collected with a home-built terahertz time domain spectroscopy system (THz-TDS) [42]. The sample is assembled on the sample holder of Oxford Instruments Spectromag He-bath cryostat, with which one could realize test environments of temperature from 10 to 300 K and magnetic field up to 7 Tesla. After propagating through these fused silica windows of the cryostat, the coverage of the THz spectral is from 0.1 to 1.5 THz. The temperature-dependent X-ray diffraction (XRD) was measured with the XRD setup using high-intensity graphite monochromatized Cu Kα radiating system (Rigaku corporation, Japan). Then, the influence of the cooling process on the copper base is excluded and finally obtain the accurate temperature-dependent evolution of the lattice constant.

Ab Initio Calculations: First-principles calculations based on density functional theory (DFT) were performed using the Vienna ab-initio simulation package (VASP) [43] with the projector-augmented wave (PAW) [44] pseudopotentials and the Perdew–Burke–Enzerhof [45] parameterization of the generalized gradient approximation (GGA). The kinetic energy cut-off was set as 400 eV. A $\Gamma$-centered 8x8x3 Monkhorst-Pack grid was used for k-point sampling, van der Waals corrections were treated by the semi-empirical DFT-D3 method. [46] Optimized atomic structures were achieved until the forces on each atom were smaller than 0.01 eV Å$^{-1}$. The phonon band structures were calculated with the frozen-phonon finite difference method using the phonopy code interfaced with VASP.

Supporting Information

Supporting Information is available from the Wiley Online Library or from the author.

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Conflict of Interest
The authors declare no conflict of interest.

Data Availability Statement
The data that support the findings of this study are available from the corresponding author upon reasonable request.

Keywords
magneto-modulation, phonon-polaritons, terahertz radiation, van der Waals materials

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