MODELING THE GRB HOST GALAXY MASS DISTRIBUTION: ARE GRBs UNBIASED TRACERS OF STAR FORMATION?

Daniel Kocevski\textsuperscript{1}, Andrew A. West\textsuperscript{2,3}, and Maryam Modjaz\textsuperscript{2,4}

\textsuperscript{1} Kavli Institute for Particle Astrophysics and Cosmology, Stanford University, 2575 Sand Hill Road M/S 29, Menlo Park, CA, 94025, USA
\textsuperscript{2} Astronomy Department, University of California, 601 Campbell Hall, Berkeley, CA, 94720, USA
\textsuperscript{3} MIT Kavli Institute for Astrophysics and Space Research, 77 Massachusetts Ave, Cambridge, MA, 02139, USA
\textsuperscript{4} Miller Research Fellow, Astronomy Department, University of California, 601 Campbell Hall, Berkeley, CA, 94720, USA

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ABSTRACT

We model the mass distribution of long gamma-ray burst (GRB) host galaxies given recent results suggesting that GRBs occur in low-metallicity environments. By utilizing measurements of the redshift evolution of the mass–metallicity relationship for galaxies, along with a sharp host metallicity cutoff suggested by Modjaz and collaborators, we estimate an upper limit on the mass of a galaxy that can efficiently produce a GRB as a function of redshift. By employing consistent abundance indicators, we find that subsolar metallicity cutoffs effectively limit GRBs to low-stellar mass spirals and dwarf galaxies at low redshift. At higher redshifts, as the average metallicity of galaxies in the Universe falls, the mass range of galaxies capable of hosting a GRB broadens, with an upper bound approaching the mass of even the largest spiral galaxies. We compare these predicted limits to the growing number of published GRB host masses and find that extremely low-metallicity cutoffs of 0.1 to 0.5 $Z_\odot$ are effectively ruled out by a large number of intermediate mass galaxies at low redshift. A mass function that includes a smooth decrease in the efficiency of producing GRBs in galaxies of metallicity above 12+log(O/H)\textsubscript{KK04} = 8.7 can, however, accommodate a majority of the measured host galaxy masses. We find that at $z \sim 1$, the peak in the observed GRB host mass distribution is inconsistent with the expected peak in the mass of galaxies harboring most of the star formation. This suggests that GRBs are metallicity-biased tracers of star formation at low and intermediate redshifts, although our model predicts that this bias should disappear at higher redshifts due to the evolving metallicity content of the universe.

Key words: gamma rays: bursts – gamma rays: observations – gamma rays: theory

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1. INTRODUCTION

The X-ray localizations of afterglows associated with long gamma-ray bursts (GRBs) have resulted in a wealth of information regarding the demographics of GRBs and their host galaxies. Investigating the environments in which these events occur has long been an important path to understanding the nature of GRB progenitors, as different origin models have traditionally predicted distinct GRB host galaxy populations. The connection between GRBs and the death of massive stars is now well established at low redshift ($z < 0.3$) by the association of GRBs with broad-lined SN Ic events (for a review, see Woosley & Bloom 2006).

Recent observations (Castro Cerón et al. 2008; Savaglio et al. 2009) of X-ray localizations by Swift have bolstered previous results showing that GRB host galaxies tend to be bluer, fainter, and more irregular than $M_*$ galaxies at similar redshifts (Fruchter et al. 1999; Chary et al. 2002; Bloom et al. 2002; Le Floc’h et al. 2003; Tanvir et al. 2004; Fruchter et al. 2006; Castro Cerón et al. 2006). They tend to have higher specific star formation than typical star-forming galaxies (Chary et al. 2002; Berger et al. 2003; Christensen et al. 2004; Castro Cerón et al. 2008) and the peak in their redshift distribution tends to broadly track the peak in the overall cosmic star-formation rate of the universe (Bloom 2003; Firmani et al. 2004; Natarajan et al. 2005; Jakobsson et al. 2006; Kocevski & Liang 2006; Guetta & Piran 2007; Li 2008). Only a handful of events have been associated with grand design spirals and no long duration GRB has been associated with an early-type galaxy. A growing body of spectroscopic evidence has also shown that these galaxies tend to be metal poor (Prochaska et al. 2004; Sollerman et al. 2005; Fruchter et al. 2006; Modjaz et al. 2006; Stanek et al. 2006; Thöne et al. 2007; Wiersema et al. 2007; Margutti et al. 2007). Absorption line spectroscopy has revealed that the regions in which GRB afterglows are observed tend to have the low metallicities that are expected from young stellar populations (Fynbo et al. 2003; Savaglio et al. 2003). However, there are a few exceptions (Fynbo et al. 2006; Modjaz et al. 2007; Fynbo et al. 2008; Chen et al. 2009). The high specific star-formation rates along with these low metallicities are similar to what are seen in star-bursting Lyman break galaxies at high redshift.

There is ample theoretical justification for the a priori association of GRBs with short-lived, metal-poor progenitors. The combination of high angular momentum and high-stellar mass at the time of collapse (Woosley 1993; MacFadyen & Woosley 1999) is crucial for producing the collimated emission that is required to account for the enormous isotropic-equivalent energy released by these events. Low-metallicity progenitors would, in theory, retain more of their mass due to smaller line-driven stellar winds (Kudritzki & Puls 2000; Vink & de Koter 2005), and hence preserve their angular momentum (Yoon & Langer 2005; Woosley & Heger 2006).

Recently, Modjaz et al. (2008) showed that a sharp delineation may exist between the metallicity at the sites of broad-lined SN Ic that have been associated with GRBs and SN Ic without detected gamma-ray emission. Using a sample of 12 nearby ($z < 0.14$) broad-lined SN Ic without associated GRBs, they
found that the chemical abundance at the sites of known supernova (SN)–GRBs (at $z < 0.25$) were systematically lower than those harboring SN without GRBs, with a boundary between the two samples at an oxygen abundance of roughly $12 + \log(O/H)_{\text{Kewley}} \sim 8.5$ in the Kewley & Dopita (2002) scale (see Modjaz et al. 2008, Figure 5). This trend is independent of the choice of the metallicity diagnostic they adopt (see their Figure 6) and the mode of SN survey that found the SN without GRBs.

At the same time, the observed trend that many GRB host galaxies are less luminous, metal poor, irregular dwarf galaxies is in qualitative agreement with the observed trend of decreasing metallicity of galaxies as a function of their stellar mass: the mass–metallicity (M-Z) relationship. Although well established, this trend between the heavy-element abundance in H II regions is in the Keyley&Dopita (2002) scale $\sim 5$ in the high-redshift universe.

As a consequence of the M-Z relationship, any bias in the metallicity of the environment that is capable of producing a GRB would likely place severe restrictions on the type of galaxies that can host such events. While earlier studies suggest that the GRB redshift distribution tends to broadly track the overall cosmic star-formation rate of the universe, the question remains as to what extent GRB hosts are unbiased tracers of SF in the high-redshift universe.

The primary question we ask is whether GRBs occur in low-mass galaxies because that is where most of the star formation is occurring at low redshifts or if they preferentially occur in these galaxies because of the low-metallicity nature of their hosts. The degeneracy between these two scenarios is broken with increasing redshift, where the metallicity of all galaxies begins to fall.

In this paper, we use empirical models based on the measurements of the redshift evolution of the M-Z relationship to estimate the upper limit to the stellar mass of a galaxy that can harbor a GRB, and test the suggestion that GRBs preferentially form in low-metallicity environments. We detail the prescriptions for our model in Section 2 and expand upon our results in Section 3. We compare our model predictions with published host mass values in Section 4 and discuss the implications of our results in Section 5.

2. MODEL PRESCRIPTIONS

To investigate how a potential metallicity cutoff affects the resulting GRB host mass distribution, we must first assume an empirical prescription for the relationship between a galaxy’s stellar mass and its level of chemical enrichment. Such a correlation was first observed by Lequeux et al. (1979); a trend between the heavy-element abundance in H II regions and the stellar mass of irregular and blue compact galaxies. More recently, this correlation has been statistically quantified by Tremonti et al. (2004) using ~53,000 galaxies from the Sloan Digital Sky Survey (SDSS). Tremonti et al. (2004) find a tight correlation between galactic stellar mass and gas-phase metallicity that spans three orders of magnitude in stellar mass and a factor of 10 in metallicity. They conclude that the galactic metallicity abundance rises steeply for stellar masses between $10^{8.5}$ and $10^{10.5} M_\odot$, then flattens for galaxies above $10^{10.5} M_\odot$.

A basic form of this correlation is a natural consequence of the conversion of gas to stars within star-forming galaxies, given a mass-dependent star-formation efficiency (Schmidt 1963; Searle & Sargent 1972). In the context of these simple “closed-box” models, this disparity in the efficiency between high- and low-mass galaxies is thought to be due to variations in galactic surface densities as a function of mass (Kennicutt 1998; Martin & Kennicutt 2001; Dalcanton et al. 2004).

It has now become apparent that the effects of SNe feedback and the infall of metal-poor gas (Dalcanton 2007) must also play important roles in shaping the observed mass–metallicity relationship. Galactic winds produced by SNe work to strip galaxies of metal-enriched gas, with low-mass galaxies being more susceptible to such effects due to their shallower potential wells. Energy injection from SNe also heats interstellar gas, delaying the collapse of otherwise cold gas to produce stars. At the same time, the infall of metal-poor gas acts to dilute the metal content of the interstellar medium (ISM). This effect is significant in small galaxies where the infall rate can exceed the total star-formation rate, causing a net decrease in the metallically of the ISM with time. The combined result of these mechanisms is that high-mass galaxies process their primordial gas faster and more efficiently than low-mass galaxies and are more effective at retaining the resulting material against wind-induced mass loss, leading to a positive correlation between stellar mass and metallicity.

These explanations for the origin of the M-Z relationship suggest significant evolution of the relationship with redshift. First, one would expect the normalization of the relationship to fall as a function of look-back time as metal abundance becomes less common in all galaxies. Second, the variations in the efficiency of star formation as a function of mass should also change the slope of the M-Z relationship as a function of redshift. Efforts to quantify this evolution have been the focus of several recent observational (Savaglio et al. 2005; Erb et al. 2006; Maiolino et al. 2008) and numerical (de Rossi et al. 2007; Kobayashi et al. 2007; Tassis et al. 2008; Brooks et al. 2007) investigation. In particular, Savaglio et al. (2005) used the Gemini Deep Deep Survey (GDDS) to examine the M-Z relationship at $0.4 < z < 1.0$ and found clear evidence for an overall decrease in the normalization of the relationship with respect to that found in the local Universe. Likewise, Erb et al. (2006) utilized 87 rest-frame UV selected star-forming galaxies to study the nature of the correlation beyond a redshift of two and came to similar conclusions.

For our analysis, we have adopted the empirical model put forth by Savaglio et al. (2005) to describe the evolution of the M-Z relationship as a function of redshift. This model was developed using their $0.4 < z < 1.0$ GDDS sample along with the $z \sim 2$ galaxies presented by Shapley et al. (2004) to extrapolate the shape of the M-Z relationship to higher redshifts. This empirical relationship (Equation (11) of Savaglio et al. 2005) allows for the average metallicity of a galaxy to be estimated as a function of stellar mass at a given redshift and can be stated as

$$12 + \log(O/H)_{\text{KK04}} = -7.59 + 2.53 \log M_\star - 0.096 \log^2 M_\star + 5.17 \log^2 t_H - 0.39 \log t_H - 0.40 \log H_0 \log M_\star,$$

where $t_H$ is the Hubble time and $M_\star$ is the galactic stellar mass. The Savaglio et al. model reproduces several of the predicted M-Z relationship properties at high redshift, including the overall reduction in the M-Z relationship normalization as well as a steeper evolution in the metallicity of low-mass galaxies in comparison to their high-mass counterparts. Figure 1 shows the
metallicity as a function of stellar mass for a variety of redshifts as approximated by the Savaglio et al. model out to z = 5. We note that the original data used by Savaglio et al. (2005) were limited to the range of 8.2 < 12+log(O/H)KK04 < 9.1 and 0.4 < z ≤ 2.0 and, hence, the curves at lower metallicities and higher redshifts are extrapolations beyond the range of the data used to define the model.

It is important to examine the details of the diagnostics used by Savaglio et al. (2005), as different initial mass functions (IMFs), for example, can yield factor of two differences in stellar mass and different metallicity calibrators can lead to a factor of 0.7 dex variance (Kewley & Ellison 2008) in the absolute metallicity scale used to measure the M-Z relationship. The stellar masses used by Savaglio et al. (2005) to produce their empirical relationship were estimated through spectral energy distribution (SED) modeling of multiband photometry for each galaxy, with an initial mass function derived by Baldry & Glazebrook (2003). Their metallicity values were obtained through nebular oxygen abundance estimates calibrated via stellar population synthesis and photoionization models developed by Kobulnicky & Kewley (2004, hereafter KK04). This metallicity diagnostic, which uses traditional strong emission line ratios, and other commonly used calibrations (e.g., McGaugh 1991; Kewley & Dopita 2002) are discussed in detail by Kewley & Ellison (2008), who quantify the systematic offsets amongst the different calibrations and provide conversion tables.

We also note that the metallicity value for the boundary between hosts that harbor broad-lined SN Ic with associated GRBs and SN Ic with no detected gamma-ray activity reported by Modjaz et al. (2008) was measured using the diagnostic proposed by Kewley & Dopita (2002, hereafter KD02). In order to convert from the KD02 scale to the KK04 scale used by Savaglio et al. (2005), we consulted Kewley & Ellison (2008) for the appropriate metallicity calibration conversion (see their Table 3). We find that a value of 12+log(O/H)KK04 = 8.5 approximately converts to 12+log(O/H)KK04 = 8.66, which we quote as the Modjaz et al. (2008) cutoff metallicity for the remainder of the paper.

In addition to understanding how the average metallicity of a galaxy varies as a function of stellar mass, we would also like to know how the number density of galaxies and the number of stars being produced in those galaxies vary with galactic stellar mass. This will allow us to model the effects of a metallicity bias on the overall mass distribution of GRB host galaxies, and eventually compare those models to the unbiased mass distribution of all star-forming galaxies at a given redshift. As with the mass–metallicity relation, both the galactic stellar mass function (GSMF) and the star-formation rate as a function of stellar mass are expected to evolve with redshift and quantifying this evolution is crucial to understanding the distribution of galaxies that are capable of harboring a GRB.

The star-formation rate as a function of stellar mass (SFRM) in the local universe is well constrained. Using a sample of more than 10^5 galaxies, Kauffmann et al. (2004) showed that the star-formation rate in low-mass galaxies scales as a power law to their halo mass, peaking at roughly log M⋆ ≈ 10.4 M⊙, before falling for higher mass galaxies. This transition represents the stellar mass at which the galaxy distribution changes from younger stellar populations and active star-forming galaxies to systems with older stellar populations and low star-formation activity.

Drory & Alvarez (2008) used the FORS Deep Field survey (Feulner et al. 2005) to quantify this relationship and its evolution with redshift for stellar masses and redshifts spanning 9 < log M⋆ < 12 and 0 < z < 5. They find that the stellar mass at which the star-formation rate turns over for high-mass galaxies evolves smoothly to higher masses with increasing redshift, until the break mass disappears entirely and the star-formation rate as a function of stellar mass can be represented as a single power law. Surprisingly, Drory & Alvarez (2008) find that the power-law index representing the low-mass region of this relationship remains constant even to the highest redshifts in their sample.

For the purposes of this paper, we have adopted the analytic expression presented by Drory & Alvarez (2008) for the star-formation rate as a function of stellar mass given as

\[ M_\star(M_\star) = M_\star^0 \left(\frac{M_\star}{M_\star^1}\right)^\beta \exp\left(-\frac{M_\star}{M_\star^0}\right), \]  

where M_\star^0 represents the break mass at which the star-formation rate deviates from a power law. We also use the best-fit parameterizations from Drory & Alvarez (2008) for the evolution of the overall normalization and break mass with redshift, given as

\[ M_\star^0 \approx 3.01(1 + z)^{3.03}, \]  

\[ M_\star^1 \approx 2.7 \times 10^{10}(1 + z)^{2.1}. \]

Following Drory & Alvarez (2008), we have fixed the power-law index to \( \beta = 0.6 \) and assume it remains constant at all redshifts under consideration. The star-formation rate as a function of stellar mass between 0 < z < 5, as described by Equations (2)–(4), is shown in Figure 2.

The GSMF in the local universe is likewise well understood. It has long been known that dwarf galaxies represent the largest fraction of galaxies in the local universe, with their relative number decreasing as a power law with increasing stellar mass up to some characteristic mass, above which the number of galaxies drops sharply. At low redshift, the 2dF (Cole et al. 2001) and Two Micron All Sky Survey (2MASS)–SDSS (Bell et al. 2003; Blanton et al. 2003) surveys constrained the parameters of the Schechter function that is commonly used to describe the distribution of stellar mass in the Universe. The GSMF
at high redshift has been explored by Fontana et al. (2004),
Drory et al. (2005), Conselice et al. (2005), and Fontana et al.
(2006) using a variety of deep surveys, all showing evidence
for a distinct evolution of the GSF with cosmic time. Using
the GOODS–MUSIC catalog of over 3000 infrared-selected
galaxies, Fontana et al. (2006) showed that the number density
of high-mass galaxies drops with redshift, while the density of low-
mass galaxies evolves faster than their high-mass counterparts
out to a redshift of \( z \sim 1.5 \). The net result of this differential
evolution is an increasing fraction of low-mass dwarf galaxies
with respect to higher mass galaxies at higher redshifts.

For the purposes of this paper, we have adopted the analytic
model presented by Drory & Alvarez (2008) for the GSFM
given as

\[
\phi(M) \, dM = \phi^*(M/M^*)^\alpha \exp\left(-\frac{M}{M^*}\right) \, dM^*.
\] (5)

We have again used their best-fit parameterizations for the
evolution of normalization of the mass function as well as the
characteristic break mass, given as

\[
\phi^*(z) \approx 0.0031(1 + z)^{-1.07},
\] (6)

\[
\log(M^*(z)) \approx 11.35 - 0.22\ln(1 + z).
\] (7)

We further assumed that the power-law index below the break
mass remains constant at \( \alpha = -1.3 \) for all redshifts under
consideration. The GSFM between \( 0 < z < 5 \), as described by
Equations (5)–(7), is shown in Figure 3.

Ultimately, it is important to know the total number of stars
being produced as a function of stellar mass. Thus, we also
computed the product of the GSF and SFRM. This galaxy-weighted
star-formation rate (WSFR) is shown in Figure 4 at a variety of redshifts.
The red lines in Figure 4 represent the metallicity-biased WSFR, the details of which
are discussed in the next section. Between roughly \( 0 < z < 3 \), the number density of low-mass galaxies outweighs
that of their more massive counterparts, but the cosmic star-
formation rate is largely dominated by these relatively less
numerous massive galaxies. The net result is a weighted star-
formation rate that peaks at intermediate masses, roughly
between \( 10^{10} \) and \( 10^{11} \, M_\odot \). At higher redshifts, the drop in
the number of high-mass galaxies becomes significant and the
stellar mass function becomes dominated by low-mass galaxies.
At the same time, the peak in the SFRM decreases smoothly to
lower masses with increasing redshift, resulting in a sharp fall

\footnotetext{We assume a solar metallicity of \( 12 + \log(O/H) = 8.7 \) (Asplund 2005) in the
Pettini & Pagel (2004) scale and convert that value to the KK04 scale using
Table 3 of Kewley & Ellison (2008) to get \( Z_\odot = 9.0 \).}
under consideration, which is certainly an oversimplification. The region of stellar mass shaded blue and green represents the typical masses for dwarf and spiral galaxies, respectively. As expected, the average mass of a galaxy at a given metallicity rises as a function of redshift, a direct effect of the decreasing normalization of the M-Z relationship as a function of look-back time. The effects this would have on a metallicity-biased GRB host population are immediately apparent. If GRBs are limited to low-metallicity environments, then at low redshift they would be relegated to dwarf and low-mass spiral galaxies (barring the effects of metallicity gradients, which we will discuss in detail in Section 5), whereas at high redshift the effective mass limit is raised, allowing GRBs to occur in a much broader range of galaxies. A similar prediction was made by Ramirez-Ruiz et al. (2002), based purely on theoretical grounds.

Furthermore, if GRBs are unbiased tracers of star formation throughout the universe, then their observed host mass distribution should cluster about the peak in the WSFR represented by the long dashed line in Figure 5. On the other hand, if they are metallicity-biased tracers of star formation, then their host mass distribution should deviate significantly from this curve at low redshifts, peaking instead at the upper mass limit shown in red. At some redshift (roughly \( z \sim 3 \)) for a metallicity cutoff of \( 12+\log(O/H)_{KK04} = 8.5 \) the stellar mass at which the WSFR peaks crosses this upper mass limit, after which the peak in the unbiased and biased mass distributions becomes indistinguishable.

We also quantified the median of the GRB host mass distribution by considering only the product of the GSMF and SFRM below the metallicity-imposed upper mass limit to the GRB host population. The red solid lines shown in Figure 4 represent the galaxy masses which fall below the upper limit imposed by a metallicity cutoff of \( 12+\log(O/H)_{KK04} = 8.5 \) for various redshifts. If GRBs are metallicity-biased tracers of the star formation in the universe, then the centroid of this truncated total star-formation rate would yield the expected median stellar mass of a GRB host population as a function of redshift. We plot this expected median mass as a dash-dotted black line in Figure 5. Although the upper limit imposed on the mass of a galaxy that can host a GRB increases with redshift, the effects of a galaxy population dominated by low-mass galaxies along with the shift in the type of galaxies producing most of the stars in the early universe have the net effect of keeping the median GRB host galaxy mass relatively constant with redshift, roughly at a mass of \( 10^9 \, M_\odot \).

Note that this estimate assumes that the fraction of the total star formation that goes into the production of GRB progenitors does not change significantly with redshift, host type, or stellar mass. This assumption breaks down if environmental variables other than metallicity play an important role in the formation of a GRB progenitor. Also, these estimates do not address the rate or overall normalization in the GRB host mass distribution, only their relative distribution in stellar galactic mass at a given redshift.

Unfortunately, the predicted median host mass shown by the dash-dotted line in Figure 5 is not currently observable, except for low redshift GRBs, which are rare. Detection effects and Malquist-type biases will lead any observational measure of the GRB host mass distribution to be biased toward high mass, high surface brightness, galaxies. This would effectively shift the dash-dotted line in Figure 5 to higher masses with increasing redshift and such completeness considerations have not been incorporated into our model.

4. COMPARISON TO GRB HOST GALAXY OBSERVATIONS

How do the upper mass limits as inferred from the M-Z relationship compare to measured values for the subset of the GRBs with known host associations? To examine this question, we turned to two recent studies by Castro Cerón et al. (2008, hereafter CC08) and Savaglio et al. (2009, hereafter SGB09), which compiled the galactic stellar masses, star-formation rates, and dust extinctions for a large sample of GRB host galaxies between \( 0 < z < 2 \). CC08 utilized the rest-frame K-band flux densities as interpolated from Spitzer’s (Werner et al. 2004) IRAC (Fazio et al. 2004) and additional NIR observations to obtain an estimate of \( M_* \) for a sample of 30 long-duration GRBs. SGB09 obtained similar estimates through a combination of optical and NIR observations for a sample of 46 host galaxies. Both groups used photometric observations in conjunction with mass-to-light ratios derived from SED fits to measure the total stellar mass of the hosts in their sample. The two studies assumed slightly different IMFs and average mass-to-light ratios, introducing a systematic offset between the estimated mass values derived from the two samples which we discuss in more detail in the next section.

CC08 and SGB09 found that GRB host galaxies exhibit a wide range of stellar mass and star-formation rates, although as a whole they tend toward low \( M_* \) relatively dim, high specific star-forming systems, confirming previous observations (Fruchter et al. 1999; Le Floc’h et al. 2003; Chary et al. 2002; Berger et al. 2003; Castro Cerón et al. 2006). The \( M_* \) values from the CC08 and SGB09 papers are shown in Figures 6 and 7, respectively, with upper limits represented by triangular symbols. As in Figure 5, the red shaded region in both plots
represents the upper limit on the stellar mass of a galaxy capable of hosting a GRB as imposed by the M-Z relationship and its associated 1σ scatter with a metallicity cutoff of $12\log(O/\text{H})_{\text{KK04}} = 8.5$. It is clear from Figures 6 and 7 that a significant fraction of observed host galaxies have $M_*$ values that are greater than the predicted upper limit to the GRB host mass distribution for such a low-metallicity cutoff value. Most of these host galaxies can be accommodated if the metallicity cutoff is increased to $12\log(O/\text{H})_{\text{KK04}} = 8.7$ for the SGB09 sample and $12\log(O/\text{H})_{\text{KK04}} = 8.8$ for the CC08 sample. Note that the resulting spread in the predicted mass range is significantly wider for $12\log(O/\text{H})_{\text{KK04}} = 8.8$ due to the shallower slope of the shallower M-Z relationship at this metallicity. Even at this relatively high-metallicity cutoff, with its larger intrinsic spread, two hosts in the CC08 sample are still above the predicted mass limit, although metallicity gradients within these high-mass hosts may explain their existence in the GRB sample.

SGB09 and CC08 found median masses of $M_* \sim 10^{9.3} M_\odot$ and $M_* \sim 10^{9.7} M_\odot$, respectively, far greater than the median host mass predicted by simply looking at the truncated distribution of total star formation as a function of $M_*$ (the dash-dotted line in Figure 5). This direct comparison between the expectation peak of the WSFR and the median values for the two samples is problematic, as detection effects biasing against low-mass galaxies will heavily influence the observed median mass. We can, however, compare the observed host mass distribution to the high end of the expected mass distribution of all star-forming galaxies at a given redshift, as detection effects should not affect this region of the observed distribution. We address this question in Figures 8 and 9, where we plot the SGB09 and CC08 host mass distributions for galaxies between $0.75 < z < 1.25$ along with the expected unbiased WSFR as a function stellar mass at a $z = 1$ (the dashed line). The normalization of the distributions in these plots is arbitrary, with the peak of the predicted WSFR and the observed host mass distributions both being set to one. The bracketed arrows in Figure 9 represent galaxies for which CC08 were unable to make firm estimates on the galactic stellar mass, resulting only in upper limits accompanied with very conservative lower limits.

It is quite clear that the SGB09 sample is not well described by the expected host mass distribution of unbiased star-forming galaxies at $z = 1$. Although the SGB09 distribution can be expected to artificially fall off at low $M_*$ due to observational biases, the same cannot be said for the lack of high $M_*$ galaxies, pointing to an intrinsic decline in the GRB host population. The case for the CC08 sample is less clear. Their median stellar mass between $0.75 < z < 1.25$ of $M_* = 10^{10.23} M_\odot$ is much more consistent with the peak of the unbiased WSFR distribution, which at $z \sim 1$ peaks at $M_* = 10^{10.30} M_\odot$. This median of the CC08 sample does not include the values for which only limits exist, which work to broaden the distribution to lower $M_*$ values, making it less consistent with the model distribution.

We can statistically compare the two observed distributions to the model distribution by drawing a random set of values from the WSFR distribution, equal in size to the observed samples, to which we can perform a two-sided Kolmogorov–Smirnov (K-S) analysis. We perform this comparison for 1000 trails, using a random realization of the WSFR mass distribution in each iteration, while measuring the median probability that the model distribution and the SGB09 and CC08 samples are drawn from the same parent populations. For both the SGB09 and CC08 samples, the probability that they are randomly drawn from the unbiased WSFR distribution is quite low, $6.3 \times 10^{-12}$ and $1.6 \times 10^{-05}$ respectively. Unfortunately, the observational biases discussed above lead to the lack of completeness at low $M_*$ for both samples making the use of a traditional K-S analysis questionable. The median WSFR mass will be heavily weighted by low-mass galaxies, the smallest of which are likely not present in the SGB09 and CC08 samples because of detection effects.

At present, without an understanding of the completeness of the GRB host samples, we can only compare the peaks and the high-end behavior of the mass distributions which we believe should not be affected by observational biases. In both cases, the
SGB09 and CC08 samples peak below the unbiased peak in the galaxy-weighted star-formation rate as a function of stellar mass, although the discrepancy is much greater when considering the SGB09 sample.

5. DISCUSSION

The comparison between the stellar mass limits imposed by metallicity cutoffs and the measured $M_*$ values in the SGB09 and CC08 samples is quite telling. A low-metallicity cutoff of $12+\log(O/H)_{KK04}$ = 8.5 is disfavored by current measurements of the stellar masses of GRB host galaxies at low and intermediate redshifts. However, a comparison of observed GRB host masses still appears to favor a metallicity-biased mass distribution rather than one based solely on the mass distribution of all star-formation galaxies at similar redshifts. Increasing the metallicity cutoff to $12+\log(O/H)_{KK04} \sim 8.7$–8.8 allows for the accommodation of most of measured host masses, when factoring in the intrinsic spread of the M-Z relationship. This is in rough agreement with the metallicity cutoff found by Modjaz et al. (2008) of roughly $12+\log(O/H)_{KK04} \sim 8.66$ at low redshift ($z < 0.25$). This result is also in general agreement with recent results presented by Nuza et al. (2007), who find a comparable metallicity bias through the use of hydrodynamical cosmological simulations in conjunction with assumptions of the collapsar event rate. Nuza et al. (2007) conclude that the observed properties of GRB host galaxies are reproduced if long GRBs are limited to low-metallicity progenitors. This general conclusion has also been reached in recent work by Li (2008) and Calura et al. (2009), who have produced metallicity-biased cosmic star-formation rate models and compare their results to the existing GRB host sample.

In a similar investigation, Wolf & Podsiadlowski (2007) used the luminosity–metallicity (L-Z) relation for galaxies to compare the host galaxy luminosity distributions between CC SNe and long GRB host galaxies to the expected luminosity function of all star-forming galaxies at a given redshift. They found that although their ultraviolet-based SFR estimates reproduced the CC SNe host luminosity distribution extremely well, the same was not true for the GRB host population. They found that their model SFR estimates would have to exclude luminous, and hence high metallicity, galaxies in order to match the observed GRB host distribution. They concluded that a metallicity bias with a cutoff of roughly $12+\log(O/H)_{KK04} \sim 8.7$ would be sufficient to reproduce the observed distribution, although they stressed that they could not distinguish between a sharp cutoff or a decreasing efficiency at producing GRBs as a function of increasing host metallicity with their current data. This decreasing efficiency is more realistic than a sharp efficiency cutoff and, combined with the spread in the M-Z relationship, could explain the existence of outliers in Figures 6 and 7.

Metallicity gradients within galaxies also work to dilute observable evidence for a sharp metallicity cutoff in the galaxies that can harbor GRBs. The metallicities within disk galaxies tend to fall as a function of radius from the core (e.g., Kewley et al. 2005, and references therein) and as such the host integrated light represents an upper limit to the metallicity at the GRB location. The nearby galaxies that most closely resemble a typical GRB host galaxy at low $z$ for which we have spatially resolved spectroscopy are the Large and Small Magellanic Clouds, both of which have small internal dispersions of order 0.1 dex in oxygen abundance (Russell & Dopita 1992). This value is common for star-forming dwarf irregular galaxies in which metallicity gradients are rather negligible, although the internal dispersion as measured from H\textsc{ii} regions in larger galaxies, such as the Milky Way, can be as high as 0.3 dex (Carigi et al. 2005; Esteban et al. 2005).

The combined effects of a smooth efficiency cutoff and this relatively small expected metallicity gradient on the GRB mass distribution are shown as dash-dotted lines in Figures 8 and 9. The upper mass limits due to sharp metallicity cutoffs are
marked by the filled red, green, and blue dots as labeled. The dash-dotted lines proceeding each limit represents the unbiased WSFR distribution convolved with a smoothly broken power-law decline in the efficiency of producing a GRB at a given metallicity, and hence stellar mass. Any effect of a metallicity gradient in a typical host galaxy would work to extend the peak of the Z-biased mass distribution to higher masses. We assumed that at low \( M_* \) values, the cutoff efficiency is one, transitioning sharply as \( M_* \rightarrow M_{\text{cutoff}} \) to a power-law decline of index \( \alpha = -1 \). We believe that such a power-law index can accommodate the spread in allowable metallicities from both the effects of a declining efficiency and the small metallicity dispersion expected in GRB host galaxies.

In the context of these two effects, the resulting \( M_{\text{cutoff}} \) now can be understood as the peak in the predicted GRB host mass distribution at low redshift and not a sharp upper limit. As such, this smooth decrease in efficiency can accommodate host galaxies of much higher stellar mass than the scatter in the M-Z relationship alone. At a metallicity cutoff of \( 12+\log(O/H)_{\text{KK04}} = 8.7 \), for example, galaxies of \( M_* \sim 10^{11} M_\odot \) are permitted by the model (in relative abundance), whereas the scatter in the M-Z relationship with a sharp efficiency cutoff would strictly exclude galaxies above \( M_* \sim 10^{10} \) at a \( z \sim 1 \). A cutoff of \( 12+\log(O/H)_{\text{KK04}} \sim 8.7 \), or 1/2 \( Z_\odot \), does contain most of the CC08 sample, although the low-mass location of the peak in the SGB09 sample points to a systematic difference between the two samples. The two host samples have a total of 25 overlapping objects, and CC08 discussed the differences between the two studies in some detail. They concluded that the higher median mass in their sample reflects a lower mass-to-light ratio obtained from the subset of galaxies for which they performed SED fits, compared to the average value obtained by SGB09 through SED fitting to their entire host sample. They also added that the use of optical-NIR SEDs by SGB09 may underestimate the effects of dust extinction for obscured galaxies, giving rise to further discrepancies.

We also note that CC08 used a traditional Salpeter IMF (Salpeter 1955) to estimate the relative number of low mass, and hence undetected, stars within a galaxy, whereas SGB09 utilized a modified Salpeter IMF presented by Baldry & Glazebrook (2003). The host masses derived through the use of these two IMFs can differ substantially, as the traditional Salpeter IMF tends to overestimate the number of low-mass dwarf stars compared to updated models presented by Baldry & Glazebrook (2003), Kroupa (2001), and Bochanski (2008). We estimated that masses derived through the use of a Baldry & Glazebrook IMF are systematically lower by roughly 85% compared to those found through the use of a Salpeter IMF for a given mass-to-light ratio. This combined with the lower effective mass-to-light ratio used by SGB09 may explain the discrepancies between the two samples. It is important to note that Savaglio et al. (2005) explicitly used the Baldry & Glazebrook IMF to obtain the M-Z relationship parameterization that we use in Equation (1); therefore, their sample makes for a more meaningful comparison to our model.

The effects of a metallicity bias in the GRB progenitor population combined with an evolving M-Z relationship would suggest that afterglow associations with massive galaxies of \( M_* > 10^{11} M_\odot \) should be limited to high-redshift events. Unfortunately, very few host galaxies have measured masses above \( z > 2 \) to test this directly, despite the median redshift of Swift detected GRBs of \( z \sim 2.75 \), highlighting the difficulty in observing many of these high-redshift hosts. Despite this increase with redshift in the upper limit in the mass of galaxies capable of harboring a GRB, we find that an evolving galaxy population in which dwarf galaxies represent a larger fraction of the star-forming galaxies in the distance universe results in a median GRB host mass that remains fairly constant between \( 0 < z < 3 \). Above \( z > 3 \), we see this upper limit falls sharply, implying that a large fraction of GRBs at high redshift still occurs in low-mass galaxies.

Finally, if the normalization of the M-Z relationship for galaxies decreases as a function of look-back time, then there should be some redshift at which a metallicity-biased galaxy population would become indistinguishable from the star-forming field galaxy population. For a metallicity cutoff of \( 12+\log(O/H)_{\text{KK04}} = 8.7 \), we find that the peak in the stellar mass distributions between these two populations should become equal at a redshift of \( z \sim 2 \), with the biased and unbiased populations becoming less distinguishable at higher redshifts. The greatest discrepancy between a metallicity-biased host population and the population of all star-forming field galaxies would occur at low to intermediate redshifts. This may explain the discrepancy between high-redshift host properties reported by Chen et al. (2009) and Fynbo et al. (2008) and the properties reported by Wolf & Podsiałdowski (2007) for hosts at intermediate redshifts. Chen et al. (2009) found that the UV luminosity distribution of long GRB hosts is largely consistent with their being drawn from a UV luminosity-weighted random galaxy population at similar redshifts. Fynbo et al. (2008) reported on similar agreements when comparing the luminosity and metallicity distributions of GRB hosts to UV-selected star-forming galaxies at \( z \sim 3 \). This is in stark disagreement with the conclusions reported by Wolf & Podsiałdowski (2007), who find that a metallicity truncated field population is required to match the luminosity distribution of GRB host galaxies at redshifts of \( 0.4 < z < 1.0 \). This dichotomy between the high-redshift and low-redshift comparisons would be expected, if at some point, the two populations become indistinguishable as the average metallicity of the field galaxies falls with increasing look-back time.

6. CONCLUSIONS

We find that the dearth of massive GRB host galaxies at low and intermediate redshifts exceeds that expected from the decline in the predicted number of massive star-forming galaxies at similar redshifts. We, therefore, conclude that there is sufficient evidence to indicate that GRB host galaxies are metallicity-biased tracers of star formation at low and intermediate redshifts and suggest that this bias should disappear at higher redshifts due to the evolving metallicity content of the early universe. We find that a galaxy mass function that includes a smooth decrease in the frequency of producing GRBs in galaxies of metallicity above \( 12+\log(O/H)_{\text{KK04}} = 8.7 \) accommodates a majority of the measured host masses. This is in rough agreement with the metallicity cutoff found by Modjaz et al. (2008) of roughly \( 12+\log(O/H)_{\text{KK04}} \sim 8.66 \) at low redshift (\( z < 0.25 \)). Throughout our analysis, the modeling and subsequent metallicity comparisons have been performed in the same, consistent fashion and in the same metallicity calibration scale, in order to avoid any systematic differences between the various metallicity diagnostics used in the literature.

For a metallicity cutoff of \( 12+\log(O/H)_{\text{KK04}} \sim 8.7 \), the predicted peak in the GRB host mass distribution and the stellar mass at which the weighted star-formation rate peaks become equal at \( z \sim 2 \), with higher values of \( 12+\log(O/H)_{\text{cutoff}} \) pushing
this intersection to lower redshift. This limits the redshift range in which the differences between a metallicity-biased GRB host population and that of unbiased star-forming galaxies can be tested through direct luminosity or mass distribution comparisons. Therefore, comparisons of these distributions at low and intermediate redshifts will be crucial to further inquiries into the nature of the metallicity bias in the GRB host population.

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