In Defense of the Triplet Loss for Person Re-Identification

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Abstract

In the past few years, the field of computer vision has gone through a revolution fueled mainly by the advent of large datasets and the adoption of deep convolutional neural networks for end-to-end learning. The person re-identification subfield is no exception to this, thanks to the notable publication of the Market-1501 and MARS datasets and several strong deep learning approaches. Unfortunately, a prevailing belief in the community seems to be that the triplet loss is inferior to using surrogate losses (classification, verification) followed by a separate metric learning step. We show that, for models trained from scratch as well as pretrained ones, using a variant of the triplet loss to perform end-to-end deep metric learning outperforms any other published method by a large margin.

1. Introduction

In recent years, person re-identification (ReID) has attracted significant attention in the computer vision community. Especially with the rise of deep learning, many new approaches have been proposed to achieve this task [18, 1, 32, 6, 34, 24, 31, 8, 41, 3, 37, 42]. In many aspects person ReID is similar to image retrieval, where significant progress has been made and where deep learning has recently introduced a lot of changes. One prominent example in the recent literature is FaceNet [23], a convolutional neural network (CNN) used to learn an embedding for faces. The key component of FaceNet is to use the triplet loss, as introduced by Weinberger and Saul [33], for training the CNN as an embedding function. The triplet loss optimizes the embedding space such that data points with the same identity are closer to each other than those with different identities. A visualization of such an embedding is shown in Fig. 1.

Several approaches to person ReID have already used some variant of the triplet loss to train their models [15, 7, 22, 6, 32, 24, 26, 20, 5]. However, the recently most successful person ReID approaches argue that a classification loss, possibly combined with a verification loss, is superior for the task [5, 40, 8, 41]. Typically, these approaches train a deep CNN using one or multiple of these surrogate losses and subsequently use a part of the network as a feature extractor, combining it with a metric learning approach to generate final embeddings. Both of these losses have their problems, though. The classification loss necessitates a growing number of learnable parameters as the number of identities increases, most of which will be discarded after training. On the other hand, many of the networks trained with a verification loss have to be used in a cross-image representation mode, only answering the question “How similar are these two images?”. This makes using them for any other task,
such as clustering or retrieval, prohibitively expensive, as each probe has to go through the network paired up with every gallery image.

In this paper we show that, contrary to current opinion, a plain CNN with a triplet loss can outperform current state-of-the-art approaches on both the Market-1501 [39] and MARS [38] datasets. The triplet loss allows us to perform end-to-end learning between the input image and the desired embedding space. This means we directly optimize the network for the final task, which renders an additional metric learning step obsolete. Instead, we can simply compare persons by computing the Euclidean distance of their embeddings.

A possible reason for the unpopularity of the triplet loss is that, when applied naively, it will indeed often produce embeddings. Pare persons by computing the Euclidean distance of their metric learning step obsolete. Instead, we can simply compute the desired embedding space. This means we directly optimize the network components specifically tailored towards person ReID. Furthermore, we do not rely on any approaches such as clustering or retrieval, prohibitively expensive, as each probe has to go through the network paired up with every gallery image.

We show that, when following best practices in deep learning, networks trained from scratch can perform competitively for person ReID. Furthermore, we do not rely on network components specifically tailored towards person ReID, but train a plain feed-forward CNN, unlike many other approaches that train from scratch [1, 31, 18, 34, 24, 17]. Indeed, our networks using pretrained weights obtain the best results, but our far smaller architecture obtains respectable scores, providing a viable alternative for applications where person ReID needs to be performed on resource-constrained hardware, such as embedded devices.

2. Learning Metric Embeddings, the Triplet Loss, and the Importance of Mining

The goal of metric embedding learning is to learn a function \( f_\theta(x) : \mathbb{R}^F \rightarrow \mathbb{R}^D \) which maps semantically similar points from the data manifold in \( \mathbb{R}^F \) onto metrically close points in \( \mathbb{R}^D \). Analogously, \( f_\theta \) should map semantically different points in \( \mathbb{R}^F \) onto metrically distant points in \( \mathbb{R}^D \). The function \( f_\theta \) is parametrized by \( \theta \) and can be anything ranging from a linear transform [33, 19, 36, 22] to complex non-linear mappings usually represented by deep neural networks [7, 6, 8]. Let \( D(x, y) : \mathbb{R}^D \times \mathbb{R}^D \rightarrow \mathbb{R} \) be a metric function measuring distances in the embedding space. For clarity we use the shortcut notation \( D_{i,j} = D(f_\theta(x_i), f_\theta(x_j)) \), where we omit the indirect dependence of \( D_{i,j} \) on the parameters \( \theta \). As is common practice, all loss-terms are divided by the number of summands in a batch; we omit this term in the following equations for conciseness.

Weinberger and Saul [33] explore this topic with the explicit goal of performing \( k \)-nearest neighbor classification in the learned embedding space and propose the “Large Margin Nearest Neighbor loss” for optimizing \( f_\theta \):

\[
L_{\text{LMNN}}(\theta) = (1 - \mu)L_{\text{pull}}(\theta) + \mu L_{\text{push}}(\theta),
\]

which is comprised of a pull-term, pulling data points \( i \) towards their target neighbor \( T(i) \) from the same class, and a push-term, pushing data points from a different class \( k \) further away:

\[
L_{\text{pull}}(\theta) = \sum_{i,j \in T(i)} D_{i,j},
\]

\[
L_{\text{push}}(\theta) = \sum_{a,n, y_a \neq y_n} \left[ m + D_{a,T(a)} - D_{a,n} \right]_+ .
\]

Because the motivation was nearest-neighbor classification, allowing disparate clusters of the same class was an explicit goal, achieved by choosing fixed target neighbors at the onset of training. Since this property is harmful for retrieval tasks such as face and person ReID. FaceNet [23] proposed a modification of \( L_{\text{LMNN}}(\theta) \) called the “Triplet loss”:

\[
L_{\text{tri}}(\theta) = \sum_{a,p,n, y_a = y_p \neq y_n} \left[ m + D_{a,p} - D_{a,n} \right]_+ .
\]

This loss makes sure that, given an anchor point \( x_a \), the projection of a positive point \( x_p \) belonging to the same class
(person) $y_a$ is closer to the anchor’s projection than that of a negative point belonging to another class $y_n$, by at least a margin $m$. If this loss is optimized over the whole dataset for long enough, eventually all possible pairs $(x_a, x_p)$ will be seen and be pulled together, making the pull-term redundant. The advantage of this formulation is that, while eventually all points of the same class will form a single cluster, they are not required to collapse to a single point; they merely need to be closer to each other than to any point from a different class.

A major caveat of the triplet loss, though, is that as the dataset gets larger, the possible number of triplets grows cubically, rendering a long enough training impractical. To make matters worse, $f_0$ relatively quickly learns to correctly map most trivial triplets, rendering a large fraction of all triplets uninformative. Thus mining hard triplets becomes crucial for learning. Intuitively, being told over and over again that people with differently colored clothes are different persons does not teach one anything, whereas seeing similarly-looking but different people (hard negatives), or pictures of the same person in wildly different poses (hard positives) dramatically helps understanding the concept of “same person”. On the other hand, being shown only the hardest triplets would select outliers in the data unproportionally often and make $f_0$ unable to learn “normal” associations, as will be shown in Table 1. Examples of typical hard positives, hard negatives, and outliers are shown in the Supplementary Material. Hence it is common to only mine moderate negatives [23] and/or moderate positives [24]. Regardless of which type of mining is being done, it is a separate step from training and adds considerably overhead, as it requires embedding a large fraction of the data with the most recent $f_0$ and computing all pairwise distances between those data points.

In a classical implementation, once a certain set of $B$ triplets has been chosen, their images are stacked into a batch of size $3B$, for which the $3B$ embeddings are computed, which are in turn used to create $B$ terms contributing to the loss. Given the fact that there are up to $6B^2 - 4B$ possible combinations of these $3B$ images that are valid triplets, using only $B$ of them seems wasteful. With this realization, we propose an organizational modification to the classic way of using the triplet loss: the core idea is to form batches by randomly sampling $P$ classes (person identities), and then randomly sampling $K$ images of each class (person), thus resulting in a batch of $PK$ images.\footnote{In all experiments we choose $B$, $P$, and $K$ in such a way that $3B$ is close to $PK$, e.g. $3 \cdot 42 \approx 32 \cdot 4$.}

Now, for each sample $a$ in the batch, we can select the hardest positive and the hardest negative samples within the batch when forming the triplets for computing the loss, which we call Batch Hard:

$$
\mathcal{L}_{BH} (\theta; X) = \sum_{p=1}^{P} \sum_{a=1}^{K} \left[ m + \max_{p=1...K} D \left( f_0(x^a_p), f_0(x^p_a) \right) \right] + \min_{j=1...P, n=1...K} D \left( f_0(x^j_a), f_0(x^n_n) \right),
$$

which is defined for a mini-batch $X$ and where a data point $x^i_j$ corresponds to the $j$-th image of the $i$-th person in the batch.

This results in $PK$ terms contributing to the loss, a threefold increase over the traditional formulation. Additionally, the selected triplets can be considered moderate triplets, since they are the hardest within a small subset of the data, which is exactly what is best for learning with the triplet loss.

This new formulation of sampling a batch immediately suggests another alternative, that is to simply use all possible $PK(K - 1)$ combinations of triplets, which corresponds to the strategy chosen in [7] and which we call Batch All:

$$
\mathcal{L}_{BA} (\theta; X) = \sum_{i=1}^{P} \sum_{a=1}^{K} \sum_{p=1}^{K} \sum_{j=1}^{P} \sum_{n=1}^{K} \left[ m - \max_{j,a,n} \min_{j,a,n} D \left( f_0(x^a_j), f_0(x^j_n) \right) \right],
$$

At this point, it is important to note that both $\mathcal{L}_{BH}$ and $\mathcal{L}_{BA}$ still exactly correspond to the standard triplet loss in the limit of infinite training. Both the max and min functions are continuous and differentiable almost everywhere, meaning they can be used in a model trained by stochastic (sub-)gradient descent without concern. In fact, they are already widely available in popular deep-learning frameworks for the implementation of max-pooling and the ReLU [9] non-linearity.

Most similar to our batch hard and batch all losses is the Lifted Embedding loss [25], which fills the batch with triplets but considers all but the anchor-positive pair as negatives:

$$
\mathcal{L}_{L} (\theta; X) = \sum_{(a,p) \in X} D_{a,p} + \log \sum_{n \neq a, n \neq p} \left( e^{m-D_{a,n}} + e^{m-D_{p,n}} \right).
$$

While [25] motivates a “hard”-margin loss similar to $\mathcal{L}_{BH}$ and $\mathcal{L}_{BA}$, they end up optimizing the smooth bound of it given in the above equation. Additionally, traditional $3B$\footnote{Because $PK \approx 3B$, see footnote 2}
batches are considered, thus using all possible negatives, but only one positive pair per triplet. This leads us to propose a generalization of the Lifted Embedding loss based on $PK$ batches which considers all anchor-positive pairs as follows:

$$
L_{LG} (\theta ; X) = \sum_{i=1}^{P} \sum_{n=1}^{K} \sum_{a=1}^{K} \log \sum_{p=1}^{K} e^{D(f_{\theta}(x_{a}), f_{\theta}(x_{p}^{j}))} - \log \sum_{j=1}^{P} \sum_{n=1}^{K} e^{m - D(f_{\theta}(x_{a}^{j}), f_{\theta}(x_{n}^{j}))} + \varepsilon,
$$

**Distance Measure.** Throughout this section, we have referred to $D(a, b)$ as the distance function between $a$ and $b$ in the embedding space. In most related works, the squared Euclidean distance $D(f_{\theta}(x_{i}), f_{\theta}(x_{j})) = \| f_{\theta}(x_{i}) - f_{\theta}(x_{j}) \|_{2}^{2}$ is used as metric, although nothing in the above loss definitions precludes using any other (sub-)differentiable distance measure. While we do not have a side-by-side comparison, we noticed during initial experiments that using the squared Euclidean distance made the optimization more prone to collapsing, whereas using the actual (non-squared) Euclidean distance was more stable. We hence used the Euclidean distance throughout all our experiments presented in this paper. In addition, squaring the Euclidean distance makes the margin parameter less interpretable, as it does not represent an absolute distance anymore. Note that when forcing the embedding’s norm to one, using the squared Euclidean distance corresponds to using the cosine-similarity, up to a factor of two.

**Soft-margin.** The role of the hinge function $[m + \cdot]_{+}$ is to avoid correcting “already correct” triplets. But in person ReID, it can be beneficial to pull together samples from the same class as much as possible [36, 6], especially when working on tracklets such as in MARS [38]. For this purpose, it is possible to replace the hinge function by a smooth approximation using the softplus function:

$$
s(x) = \log(1 + \exp(x)),
$$

for which numerically stable implementations are commonly available as $\text{log1p}$. The softplus function has similar behavior to the hinge, but it decays exponentially instead of having a hard cut-off, we hence refer to it as the soft-margin formulation.

**Summary.** In summary, the novel contributions proposed in this paper are the batch hard loss and its soft margin version. In the following section we evaluate them experimentally and show that, for ReID, they achieve superior performance compared to both the traditional triplet loss and the previously published variants of it [7, 25].

### 3. Experiments

Our experimental evaluation is split up into three main parts. The first section evaluates different variations of the triplet loss, including some hyper-parameters, and identifies the setting that works best for person ReID. This evaluation is performed on a train/validation split we create based on the MARS training set. The second section shows the performance we can attain based on the selected variant of the triplet loss. We show state-of-the-art results on both the Market-1501 and MARS test sets, based on a pretrained network and a network trained from scratch. Finally, the third section discusses advantages of training models from scratch with respect to real-world use cases.

#### 3.1. Datasets

We focus on the Market-1501 [39] and MARS [38] datasets, the two largest person ReID datasets currently available. The Market-1501 dataset contains bounding boxes from a person detector which have been selected based on their intersection-over-union overlap with manually annotated bounding boxes. It contains 32,668 images of 1501 persons, split into train/test sets of 12,936/19,732 images as defined by [39]. The dataset uses both single- and multi-query evaluation, we report numbers for both.

The MARS dataset originates from the same raw data as the Market-1501 dataset; however, a significant difference is that the MARS dataset does not have any manually annotated bounding boxes, reducing the annotation overhead. MARS consist of “tracklets” which have been grouped into person IDs manually. It contains 1,191,003 images split into train/test sets of 509,914/681,089 images, as defined by [38]. Here, person ReID is no longer performed on a frame-to-frame level, but instead on a tracklet-to-tracklet level, where feature embeddings are pooled across a tracklet, thus it is inherently a multi-query setup.

We use the standard evaluation metrics for both datasets, namely the mean average precision score (mAP) and the cumulative matching curve (CMC) at rank-1 and rank-5. To compute these scores we use the evaluation code provided by [43].

#### 3.2. Training

Unless specifically noted otherwise, we use the same training procedure across all experiments and on all datasets. We performed all our experiments using the Theano [4] framework, all code is available at https://github.com/VisualComputingInstitute/triplet-reid.

We use the Adam optimizer [16] with the default hyperparameter values ($\epsilon = 10^{-3}$, $\beta_1 = 0.9$, $\beta_2 = 0.999$) for
most experiments. During initial experiments on our own MARS validation split (see Sec. 3.4), we ran multiple experiments for a very long time and monitored the loss and mAP curves. With this information, we decided to fix the following exponentially decaying training schedule, which does not disadvantage any setup, for all experiments presented in this paper:

\[
\epsilon(t) = \begin{cases} 
\epsilon_0 & \text{if } t \leq t_0 \\
\epsilon_0 0.001 \frac{t-t_0}{t_1-t_0} & \text{if } t_0 \leq t \leq t_1 
\end{cases}
\]

(9)

with \(\epsilon_0 = 10^{-3}\), \(t_0 = 15,000\), and \(t_1 = 25,000\), stopping training when reaching \(t_1\). We also set \(\beta_1 = 0.5\) when entering the decay schedule at \(t_0\), as is common practice [2].

### 3.3. Network Architectures

For our main results we use two different architectures, one based on a pretrained network and one which we train from scratch.

- **Pretrained.** We use the ResNet-50 architecture and the weights provided by He et al. [12]. We discard the last layer and add two fully connected layers for our task. The first has 1024 units, followed by batch normalization [14] and ReLU [9], the second goes down to 128 units, our final embedding dimension. Trained with our batch hard triplet loss, we call this model TriNet. Due to the size of this network (25.74 M parameters), we had to limit our batch size to 72, containing \(P = 18\) persons with \(K = 4\) images each. For these pretrained experiments, \(\epsilon_0 = 10^{-3}\) proved to be too high, causing the models to diverge within few iterations. We thus reduced \(\epsilon_0\) to \(3 \cdot 10^{-4}\) which worked fine on both datasets.

- **Trained from Scratch.** To show that training from scratch does not necessarily result in poor performance, we also designed a network called LuNet which we train from scratch. LuNet follows the style of ResNet-v2, but uses leaky ReLU nonlinearities, multiple \(3 \times 3\) max-poolings with stride 2 instead of strided convolutions, and omits the final average-pooling of feature-maps in favor of a channel-reducing final res-block. An in-depth description of the architecture is given in the Supplementary Material and the accompanying source-code. As the network is much more lightweight (5.00 M parameters) than its pretrained sibling, we sample batches of size 128, containing \(P = 32\) persons with \(K = 4\) images each.

### 3.4. Triplet Loss

Our initial experiments test the different variants of triplet training that we discussed in Sec. 2. In order not to perform model-selection on the test set, we randomly sample a validation set of 150 persons from the MARS training set, leaving the remaining 475 persons for training. In order to make this exploration tractable, we run all of these experiments using the smaller LuNet trained from scratch on images downscaled by a factor of two. Since our goal here is to explore triplet loss formulations, as opposed to reaching top performance, we do not perform any data augmentation in these experiments.

Table 1 shows the resulting mAP and rank-1 scores for the different formulations at multiple margin values, and with a soft-margin (Eq. 8) where applicable. Consistent with results reported in several recent papers [8, 7, 5], the vanilla triplet loss with randomly sampled triplets performs poorly. When performing simple offline hard-mining (OHM), the scores sometimes increase dramatically, but the training also fails to learn useful embeddings for multiple margin values. This problem is well-known [23, 24] and has been discussed in Sec. 2. While the idea of learning embeddings using triplets is theoretically pleasing, this practical finnickyness, coupled with the considerable increase in training time due to non-parallelizable offline mining (from 7 h to 20 h in our experiments), makes learning with vanilla triplets rather unattractive.

Considering the long training times, it is nice to see that
| Type                        | Market-1501 SQ | Market-1501 MQ | MARS               |
|-----------------------------|----------------|----------------|--------------------|
|                            | mAP | rank-1 | rank-5 | mAP | rank-1 | rank-5 | mAP | rank-1 | rank-5 |
| TriNet                      | E  | 69.14 | 84.92 | 94.21 | 76.42 | 90.53 | 96.29 | 67.70 | 79.80 | 91.36 |
| LuNet (R) + ML ours         | I  | 58.06 | 78.50 | 91.18 | 67.48 | 85.45 | 94.12 | 57.42 | 72.42 | 86.21 |
| LOMO + Null Space [36]      | E  | 29.87 | 55.43 | 46.03 | 49.7  | 72.4  | 48.45 | 55.12 | 70.51 | -     |
| DTL† [8]                   | I+V | 59.87 | 79.51 | 90.91 | 70.33 | 85.84 | 94.54 | -     | -     | -     |
| ResNet 50 (I+V)† [41]      | V  | 39.55 | 65.88 | 48.45 | 76.04 | -     | -     | -     | -     | -     |
| Gated siamese CNN [31]     | I  | 56.23 | 78.06 | 85.12 | -     | -     | -     | -     | -     | -     |
| CNN + DCGAN† [42]          | I  | 49.05 | 73.60 | -     | -     | -     | -     | -     | -     | -     |
| IDE (R) + ML [43]          | I  | 63.63 | 77.11 | -     | -     | -     | -     | -     | -     | -     |
| TriNet (Re-ranked)         | E  | 81.07 | 86.67 | 93.38 | 87.18 | 91.75 | 95.78 | 77.43 | 81.21 | 90.76 |
| LuNet (Re-ranked)          | E  | 75.62 | 84.59 | 91.89 | 82.61 | 89.31 | 94.48 | 73.68 | 78.48 | 88.74 |
| IDE (R) + ML ours (Re-ra.) | I  | 71.38 | 81.62 | 89.88 | 79.78 | 86.79 | 92.96 | 69.50 | 74.39 | 85.86 |
| IDE (R) + ML (Re-ra.) [43] | I  | 63.63 | 77.11 | -     | -     | -     | -     | 68.45 | 73.94 | -     |

Table 2: Scores on both the Market-1501 and MARS datasets. The top and middle contain our scores and those of the current state-of-the-art respectively. The bottom contains several methods with re-ranking [43]. The different types represent the optimization criteria, where I stands for identification, V for verification and E for embedding. All our scores include test-time augmentation. The best scores are bold. †: Concurrent work only published on arXiv.

All proposed triplet re-formulations perform similarly to or better than the best OHM run. The key observation is that the (semi) hard-mining happens within the batch and thus comes at almost no additional runtime cost.

Perhaps surprisingly, the batch hard variant (Eq. 5) consistently outperforms the batch all variant (Eq. 6) previously used by several authors [7, 32]. We suspect this is due to the fact that in the latter, many of the possible triplets in a batch are zero, essentially “washing out” the few useful contributing terms during averaging. To test this hypothesis, we also ran experiments where we only average the non-zero loss terms (marked by $\neq 0$ in Table 1); this performs much better in the batch all case. Another interpretation of this modification is that it dynamically increases the weight of triplets which remain active as they get fewer.

The lifted triplet loss $L_L$ as introduced by [25] performs competitively, but is slightly worse than most other formulations. As can be seen in the table, our generalization to multiple positives (Eq. 7), which makes it more similar to the batch all variant of the triplet, improves upon it overall.

The best score was obtained by the soft-margin variation of the batch hard loss. We use this loss in all our further triplet experiments. To clarify, here we merely seek the best triplet loss variation for person ReID, but do not claim that this variant works best across all fields. For other tasks such as image retrieval or clustering, additional experiments will have to be performed.

### 3.5. Performance on Market-1501 and MARS

Here, we present the main experiments of this paper. We perform all following experiments using the batch hard variant $L_{BH}$ of the triplet loss and the soft margin, since this setup performed best during the exploratory phase.

**Batch Generation and Augmentation.** Since our batch hard triplet loss requires slightly different mini-batches, we sample randomly $PK$-style batches by first randomly sampling $P$ person identities uniformly without replacement. For each person, we then sample $K$ images, without replacement whenever possible, otherwise replicating images as necessary. For the pretrained network, we subtract the mean pixel value used during the original network training on ImageNet, while for our own models we simply divide the RGB values by 255.

We apply test-time augmentation in all our experiments. Following [17], we deterministically average over the em-
beddings from five crops and their flips. This typically gives an improvement of 3\% in the mAP score; a more detailed explanation and analysis can be found in the Supplementary Material.

**Comparison to State-of-the-Art.** Table 2 compares our results to a selection of other approaches. To the best of our knowledge, it shows all methods reporting scores on the MARS dataset. For Market-1501, we limit the comparison to the three approaches with top scores both from arXiv and from peer-reviewed conferences. The different approaches are categorized into three major types: Identification models (I) that are trained to classify person IDs, Verification models (V) that learned whether an image pair represents the same person, and methods such as ours that directly learn an Embedding (E).

We present results for both our pretrained network (TriNet) and the network we trained from scratch (LuNet). As it can clearly be seen, TriNet easily outperforms all current methods. Especially striking is the jump from 41.5\% mAP, obtained by another ResNet-50 model trained with triplets (DTL [8]), to our 69.14\% mAP score. Since Geng et al. [8] do not discuss all details of their training procedure when using the triplet loss, we could only speculate about the reasons for the large performance gap.

Our LuNet model, which we train from scratch, also performs very competitively. Apart from DTL [8], it matches or outperforms all other baselines. While it does not quite reach the performance of our pretrained model, our results clearly show that with proper training, the flexibility of training models from scratch (see Sec. 3.6) should not be discarded.

To show that the actual performance boost is indeed gained by the triplet loss and not by other design choices, we train a ResNet-50 model with a classification loss. This model is very similar to the one used in [43] and we thus refer to it as “IDE (R) ours”, for which we also apply a metric learning step (XQDA [19]). Unfortunately, especially difficult images caused frequent spikes in the loss, which ended up harming the optimization using Adam. After unsuccessfully trying lower learning rates and clipping extreme loss values, we resorted to Adadelta [35], another competitive optimization algorithm which did not exhibit these problems. While average-pooling worked best for our triplet based models during multi-query fusion, for our classification based models we found max-pooling to work better, consistent with results reported in [38]. As Table 2 shows, the performance of the resulting model “IDE (R) ours” is still on-par with similar models in the literature. However, the large gap between the identification-based model and our TriNet clearly demonstrates the advantages of using a triplet loss.

In line with the general trend in the vision community, all deep learning methods outperform shallow methods using hand-crafted features. While Table 2 only shows [36] as a non-deep learning method, to the best of our knowledge all others perform worse.

Finally, we also evaluated how our models fare when combined with a recent re-ranking approach by Zhong et al. [43]. This approach can be applied on top of any ranking methods and uses information from nearest neighbors in the gallery to improve the ranking result. As Table 2 shows, our approaches go well with this method and show similar improvements to those obtained by Zhong et al. [43].

These results show that triplet loss embeddings are indeed a valuable tool for person ReID and we expect them to significantly change the way how research will progress in this field.

### 3.5.1 Market-1501 + 500k Distractors

On top of the normal gallery set, the Market-1501 dataset provides an additional 500k distractors recorded at another time. In order to evaluate how such distractors affect performance, we randomly sample an increasing number of distractors and add them to the original gallery set. Here we compare to the results from Zheng et al. [41]. Both our models show a similar behavior to that of their ResNet-50 baseline. Surprisingly, our LuNet model starts out with a slightly better mAP score than the baseline and ends up just below it, while consistently being better when considering the rank-1 score. This might indeed suggest that the inductive bias from pretraining helps during generalization to large amounts of unseen data. Nevertheless, all models seem to suffer under the increasing gallery set in a similar manner, albeit none of them fails badly. Especially the fact that in 74.70\% of all single-image queries the first image out of 519732 gallery images is correctly retrieved is an impressive result.
3.6. To Pretrain or not to Pretrain?

As mentioned before, many methods for person ReID rely on pretrained networks, following a general trend in the computer vision community. Indeed, these models lead to impressive results, as we also confirmed in this paper with our TriNet model. However, pretrained networks reduce the flexibility to try out new advances in deep learning or to make task-specific changes in a network. Our LuNet model clearly suggests that it is also possible to train models from scratch and obtain competitive scores.

In particular, an interesting direction for ReID could be the usage of additional input channels such as depth information, readily available from cheap consumer hardware. However it is unclear how to best integrate such input data into a pretrained network in a proper way.

Furthermore, the typical pretrained networks are designed with performance in mind and do not focus on the memory footprint or the runtime of a method. Both are important factors for real-world robotic scenarios, where typically power consumption is a constraint and only less powerful hardware can be considered [10, 29]. When designing a network from scratch, one can directly take this into consideration and create networks with a smaller memory footprint and faster evaluation times.

In principle, our pretrained model can easily be sped up by using half or quarter size input images, since the global average pooling in the ResNet will still produce an output vector of the same shape. This, however, goes hand in hand with the question of how to best adapt a pretrained network to a new task with different image sizes. The typical way of leveraging pretrained networks is to simply stretch images to the fixed expected input size used to train the network, typically $224 \times 224$ pixels. We used $256 \times 128$ instead in order to preserve the aspect ratio of the original image. However, for the Market-1501 dataset, this meant we had to upscale the images, while if we do not confine ourselves to pretrained networks we can simply adjust our architecture to the dataset size, as we did in the LuNet architecture. However, we hypothesize that a pretrained networks has an “intrinsic scale,” for which the learned filters work properly and thus simply using smaller input images will result in suboptimal performance. To show this, we retrain our TriNet with $128 \times 64$ and $64 \times 32$ images. As Table 3 clearly shows, the performance drops rapidly. At the original image scale, our LuNet model can almost match the mAP score and already outperforms it when considering CMC scores. At an even smaller image size, LuNet significantly outperforms the pretrained model. Since the LuNet performance only drops by about $\sim 3\%$, the small images still hold enough data to perform ReID, but the rather rigid pretrained weights can no longer adjust to such a data change. This shows that pretrained models are not a solution for arbitrary tasks, especially when one wants to train lightweight models for small images.

### Table 3: The effect of input size on mAP and CMC scores.

| Input Size | TriNet mAP | TriNet rank-1 | TriNet rank-5 | LuNet mAP | LuNet rank-1 | LuNet rank-5 |
|------------|------------|---------------|---------------|-----------|--------------|--------------|
| $256 \times 128$ | 69.14 | 84.92 | 94.21 | - | - | - |
| $128 \times 64$ | 62.52 | 79.45 | 91.06 | 60.71 | 81.38 | 92.34 |
| $64 \times 32$ | 47.42 | 68.08 | 85.84 | 57.18 | 78.21 | 90.94 |

#### Related Work.

We are not the first to use the triplet loss for person ReID. Ding et al. [7] and Wang et al. [32] use a batch generation and loss formulation which is very similar to our batch all formulation. Wang et al. [32] further combine it with a pairwise verification loss. However, in the batch all case, it was important for us to average only over the active triplets ($C_{BA}^{A_0}$), which they do not mention. This, in combination with their rather small networks, might explain their relatively low scores. Cheng et al. [6] propose an “improved triplet loss” by introducing another pull term into the loss, penalizing large distances between positive images. This formulation is in fact very similar to the original one by Weinberger and Saul [33]. We briefly experimented with a pull term, but the additional weighting hyper-parameter was not trivial to optimize and it did not improve our results. Khamis et al. [15] and Su et al. [26] directly integrate attributes into their embedding dimensions. This is an interesting research direction orthogonal to our work. Several other authors also defined losses over triplets of images [22, 24, 20], however, they use losses different from the triplet loss we defend in this paper, possibly explaining their lower scores.

### Notes on Network Training.

We would like to share a few notes on training that could benefit the wider community.

First, forcing the norm of the embedding to be a fixed number, e.g. one, is not necessary. For one, it does not dramatically regularize the network by reducing the available embedding space: the space spanned by all $D$-dimensional vector of fixed norm is still a $D-1$-dimensional volume. Worse, an output-normalization layer actually hides problems in the training, such as slowly collapsing or exploding embeddings. We did not use a normalizing layer in any of our final experiments.

Second, if any type of hard-triplet mining is used, a stagnating loss curve by no means indicates stagnating progress. As the network learns to solve some hard cases, it will be presented with other hard cases and hence still keep a high loss. We recommend observing the fraction of active triplets in a batch, as well as the norms of the embeddings and all pairwise distances. We show some such training logs in the Supplementary Material.
Finally, training usually proceeds as follows: initially, all embeddings are pulled together towards their center of gravity. When they come close to each other, they will “pass” each other to join “their” clusters and, once this cross-over has happened, training mostly consists of pushing the clusters further apart and fine-tuning them. The collapsing of training happens when the margin is too large and the initial spread is too small, such that the embeddings get stuck when trying to pass each other. This is also evidenced by training logs from the Supplementary Material.

5. Conclusion

In this paper we have shown that, contrary to the prevailing belief, the triplet loss is an excellent tool for person re-identification. We propose a variant that no longer requires offline hard negative mining at almost no additional cost. Combined with a pretrained network, we set the new state-of-the-art on two of the major ReID datasets. Furthermore, we show that training networks from scratch can lead to very competitive scores. We hope that in future work the ReID community will build on top of our results and shift more towards end-to-end learning.

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Supplementary Material

A. Test-time Augmentation

As is good practice in the deep learning community [17, 12], we perform test-time augmentation. From each image, we deterministically create five crops of size $H \times W$: four corner crops and one center crop, as well as a horizontally flipped copy of each. The embeddings of all these ten images are then averaged, resulting in the final embedding for a person. Table 4 shows how five possible settings affect our scores on the Market-1501 dataset. As expected, the worst option is to scale the original images to fit the network input (first line), as this shows the network an image type it has never seen before. This option is directly followed by not using any test-time augmentation, i.e. just using the central crop. Simply flipping the center crop and averaging the two resulting embeddings already gives a big boost while only being twice as expensive. The four additional corner crops typically seem to be less effective, while more expensive, but using both augmentations together gives the best results. For the networks trained with a triplet loss, we gain about 3% mAP, while the network trained for identification only gains about 2% mAP. A possible explanation is that the feature space we learn with the triplet loss could be more suited to averaging than that of a classification network.

| TriNet | LuNet | IDE (R) Ours |
|--------|-------|--------------|
| mAP    | mAP   | mAP          |
| rank-1 | rank-1| rank-1       |
| original | 65.48 | 55.61 | 56.29 |
|        | 82.51 | 76.72 | 77.55 |
| center | 66.29 | 57.08 | 56.26 |
|        | 84.06 | 77.94 | 77.08 |
| center + flip | 68.32 | 59.31 | 59.87 |
|        | 84.47 | 79.78 | 79.51 |
| 5 crops | 67.86 | 59.00 | 59.87 |
|        | 84.83 | 79.42 | 79.51 |
| 5 crops + flip | 69.14 | 60.71 | 61.94 |
|        | 84.92 | 81.38 | 81.92 |

Table 4: The effect of test-time augmentation on Market-1501.

B. Hard Positives, Hard Negatives and Outliers

Figure 3 shows several outliers in the Market-1501 and MARS datasets. Some issues in MARS are caused by the tracker-based annotations where bounding boxes sometimes span two persons and the tracker partially focuses on the wrong person. Additionally, some annotation mistakes can be found in both datasets; while some are obvious, some others are indeed very hard to spot!

In Figure 4 we show some of the most difficult queries along with their top-3 retrieved images (containing hard negatives), as well as their two hardest positives. While some mistakes are easy to spot by a human, others are indeed not trivial, such as the first row in Figure 4.

Figure 3: Some outliers in the Mars (top two rows) and Market-1501 (bottom row) datasets. The first row shows high image overlap between tracklets of two persons. The second row shows a very hard example where a person was wrongly matched across tracklets. The last row shows a simple annotation mistake.

C. Experiments with Distractors

For reproducibility of the 500k distractor plot (Fig. 2 in the paper), Table 5 lists the values of the plot.

| TriNet | LuNet | Res50 (I+V) [41] |
|--------|-------|------------------|
| Gallery size | mAP | rank-1 | mAP | rank-1 | mAP | rank-1 |
| 19732 | 69.14 | 84.92 | 60.71 | 81.38 | 59.87 | 79.51 |
| 119732 | 61.93 | 79.69 | 52.73 | 75.65 | 52.28 | 73.78 |
| 219732 | 58.74 | 77.88 | 49.44 | 73.40 | 49.11 | 71.50 |
| 319732 | 56.58 | 76.34 | 47.17 | 71.85 | NaN | NaN |
| 419732 | 54.97 | 75.50 | 45.57 | 70.52 | NaN | NaN |
| 519732 | 53.63 | 74.70 | 44.26 | 69.74 | 45.24 | 68.26 |

Table 5: Values for the 500k distractor plot.

D. LuNet’s Architecture

The details of the LuNet architecture for training from scratch can be seen in Table 6. The input image has three channels and spatial dimensions $128 \times 64$. Most Res-blocks are of the “bottleneck” type [13], meaning for given numbers $n_1, n_2, n_3$, in the table, they consist of a $1 \times 1$ con-
Figure 4: Some of the hardest queries. The leftmost column shows the query image, followed by the top 3 retrieved images and the two ground truth matches with the highest distance to the query images, i.e. the hardest positives. Correctly retrieved images have a green border, mistakes (i.e. hard negatives) have a red border.

Table 6: The architecture of LuNet.

| Type      | Size                          |
|-----------|-------------------------------|
| Conv      | $128 \times 7 \times 7 \times 3$ |
| Res-block | $128, 32, 128$                |
| MaxPool   | pool $3 \times 3$, stride $(2 \times 2)$, padding $(1 \times 1)$ |
| Res-block | $128, 32, 128$                |
| Res-block | $128, 32, 128$                |
| Res-block | $128, 64, 256$                |
| MaxPool   | pool $3 \times 3$, stride $(2 \times 2)$, padding $(1 \times 1)$ |
| Res-block | $256, 64, 256$                |
| Res-block | $256, 64, 256$                |
| MaxPool   | pool $3 \times 3$, stride $(2 \times 2)$, padding $(1 \times 1)$ |
| Res-block | $256, 512$                    |
| Res-block | $256, 512$                    |
| MaxPool   | pool $3 \times 3$, stride $(2 \times 2)$, padding $(1 \times 1)$ |
| Res-block | $512, 512$                    |
| Res-block | $512, 512$                    |
| MaxPool   | pool $3 \times 3$, stride $(2 \times 2)$, padding $(1 \times 1)$ |
| Res-block | $512 \times (3 \times 3 \times 512)$, $128 \times (3 \times 3 \times 512)$ |
| Linear    | $1024 \times 512$            |
| Batch-Norm| $512$                         |
| ReLU      |                               |
| Linear    | $512 \times 128$             |
E. Full t-SNE Visualization

Figure 5 shows the full Barnes-Hut t-SNE visualization from which the teaser image (Fig. 1 in the paper) was cropped. We used a subset of 6000 images from the Market-1501 test-set and a perplexity of 5000 for this visualization.

F. Typical Training Logs

Here we present and discuss several training-logs that display interesting behavior, as noted in the main paper. This serves as practical advice of what to monitor for practitioners who choose to use a triplet-based loss in their training.

Figures 6, 7, 8, and 9 all show different training logs.
Note that while they all share the x-axis since the number of updates was kept the same throughout the experiments, the y-axes vary for clearer visualization. First, the topmost plot in each Subfigure (a) ("Value of criterion/penalty") shows all per-triplet values of the optimization criterion (the triplet loss) encountered in each mini-batch. This is shown again in the plot below it on the left ("loss"), with an overlaid light-blue line representing the batch-mean criterion value, and an overlaid dark-blue line representing the batch’s 5-percentile. To the right of it, the “% non-zero losses in batch” shows how many entries in the mini-batch had non-zero loss; values are computed up to a precision of $10^{-5}$, which explains how it can be below 100% in the soft-margin case. The single final vertical line present in some plots should be ignored as a plotting-artifact.

Second, each Subfigure (b) (blue plots), monitors statistics about the embeddings computed during training. Different lines show 0, 5, 50, 95, and 100-percentiles within a mini-batch, thus visualizing the distribution of values. The top-left plot, “2-norm of embeddings”, shows the norms of the embeddings, thus visualizing whether the embedding-space shrinks towards 0 or expands. The top-right plot, “%tiles value of embedding entries” shows these same statistics over the individual numeric entries in the embedding vectors. The only use we found for this plot is noticing when embeddings collapse to all-zeros vs. some other value. Finally, the bottom-left plot, “Distance between embeddings”, is the most revealing, as it shows the same percentiles over all pairwise distances between the embeddings within a mini-batch.

Let us start by looking at the logs of two very successful runs: the LuNet training from scratch on Market-1501 with batch hard triplet loss with margin 0.2. The embeddings stay bounded, as expected from a triplet formulation, and there is a lot of progress even when the loss stays seemingly flat.

Figure 6: Training-log of LuNet on Market1501 using the batch hard triplet loss with margin 0.2. The embeddings keep moving apart as even the loss shows a steady downward trend.
Figure 8: Training-log of a very small net (not further specified in this paper). We can clearly see that the network first pulls all embeddings towards their center of gravity, as evidenced by the quickly decreasing embedding norms, entries, as well as distances in the first few hundred updates. (More visible when zooming-in on a computer.) Once they are all close to each other, the networks really struggles to make them all “pass each other” to reach “their” clusters. As soon as this difficult phase is overcome, the embeddings are spread around the space to quickly decrease the loss. This is where the training becomes “fragile” and prone to collapsing: if the embeddings never pass each other, training gets stuck. This behavior can also be observed in Figures 6 and 7, although to a much lesser extent, as the network is powerful enough to quickly overcome this difficult phase.

Next, let us turn to Fig. 8, which shows the training-log of a very small net (not further specified in this paper). We can clearly see that the network first pulls all embeddings towards their center of gravity, as evidenced by the quickly decreasing embedding norms, entries, as well as distances in the first few hundred updates. (More visible when zooming-in on a computer.) Once they are all close to each other, the networks really struggles to make them all “pass each other” to reach “their” clusters. As soon as this difficult phase is overcome, the embeddings are spread around the space to quickly decrease the loss. This is where the training becomes “fragile” and prone to collapsing: if the embeddings never pass each other, training gets stuck. This behavior can also be observed in Figures 6 and 7, although to a much lesser extent, as the network is powerful enough to quickly overcome this difficult phase.