\( \Xi' \) Production at \( \text{BABAR} \)

The \( \text{BABAR} \) Collaboration

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Abstract

Using 232 fb\(^{-1} \) of data collected by the \( \text{BABAR} \) detector, the \( \Xi'_c \) and \( \Xi'_c^0 \) baryons are reconstructed through the decays: \( \Xi'_c^+ \to \Xi'_c^+ \gamma \) and \( \Xi'_c^0 \to \Xi'_c^0 \gamma \), where \( \Xi'_c^+ \to \Xi^- \pi^+ \pi^+ \) and \( \Xi'_c^0 \to \Xi^- \pi^+ \). By measuring the efficiency-corrected yields in different intervals of the center-of-mass momentum, the production rates from \( \mathcal{B} \) decays and from the continuum are extracted. For production from \( \mathcal{B} \) decays, the branching fractions are found to be

\[
B(\mathcal{B} \to \Xi'_c^+ X) \times B(\Xi'_c^+ \to \Xi^- \pi^+ \pi^+) = [1.69 \pm 0.17 \text{ (exp.)} \pm 0.10 \text{ (model)}] \times 10^{-4}
\]

and

\[
B(\mathcal{B} \to \Xi'_c^0 X) \times B(\Xi'_c^0 \to \Xi^- \pi^+) = [0.67 \pm 0.07 \text{ (exp.)} \pm 0.03 \text{ (model)}] \times 10^{-4}.
\]

For production from the continuum the cross-sections are found to be

\[
s(\ell^+ \ell^- \to \Xi'_c^+ X) \times B(\Xi'_c^+ \to \Xi^- \pi^+ \pi^+) = 141 \pm 24 \text{ (exp.)} \pm 19 \text{ (model)} \text{ fb}
\]

and

\[
s(\ell^+ \ell^- \to \Xi'_c^0 X) \times B(\Xi'_c^0 \to \Xi^- \pi^+) = 70 \pm 11 \text{ (exp.)} \pm 6 \text{ (model)} \text{ fb}.
\]

The helicity angle distributions of \( \Xi'_c \) decays are studied and found to be consistent with \( J = \frac{1}{2} \).

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1 INTRODUCTION

Charmed baryons have a complex and intricate spectroscopy. The states can be classified in the following categories:

| State | Quark content | Isospin configuration |
|-------|---------------|-----------------------|
| Λ_c  | cud           | Isosinglet            |
| Σ_c  | cqq           | Isotriplet            |
| Ξ_c  | csq           | Isodoublet            |
| Ω_c  | css           | Isosinglet            |

where q indicates a u or a d quark. There are numerous states for each of these quark flavor configurations [1], several of which have been observed [2].

In this analysis, we focus on the Ξ_c states, and in particular on the lowest resonances above the ground state, the Ξ'_c. This is one of three Ξ_c states, listed below, which are not radially excited and which have zero orbital angular momentum:

| State | Approx. mass (MeV/c^2) | Light flavor wavefunction | J^P |
|-------|-------------------------|--------------------------|-----|
| Ξ_c   | 2470                    | Antisymmetric            | 1^+ |
| Ξ'_c  | 2580                    | Symmetric                | 1^+ |
| Ξ^* _c| 2645                    | Symmetric                | 3^+ |

Note that the J^P of the Ξ'_c and Ξ^*_c have not been directly measured but are assigned from the quark model predictions. In a recent study of the decay Ξ'_c → Ω^- K^+ [3], the helicity angle of the Ξ'_c was found to be consistent with J = \frac{1}{2}^+, though higher spins were not excluded.

The mass difference between the Ξ'_c and ground state is only ∆m = m(Ξ'_c) − m(Ξ_c) ≃ 107 MeV/c^2. Hence, the Ξ'_c is below threshold for a strong decay via Ξ_cπ or other final states such as Λ_cK or DΛ, and so it can only decay by photon emission, Ξ'_c → Ξ_cγ.

The Ξ'_c and Ξ^*_c states were observed by CLEO in 5.0 fb^{-1} of data [4]. This observation has not yet been confirmed by another experiment. Charmed baryons can be produced in two ways at e^+e^- B-factories: from the continuum and in decays of B mesons. The CLEO measurement was made with requirements that x_p ≥ 0.5–0.6 depending on the decay channel, where x_p ≡ p^*/\sqrt{s/4} - m^2_{Ξ'_c} and p^* is the center-of-mass momentum of the Ξ'_c. These requirements suppressed combinatorial background, but they also removed any Ξ'_c production from B-decays, retaining only the continuum production of Ξ'_c.

Recent results from BABAR and Belle indicate that B decays to charmed baryon pairs occur at a high rate even when the available phase space is small [5-9]. One possible explanation is that baryon formation is enhanced when the two baryons are almost at rest in their center-of-mass frame, and strongly suppressed when their relative motion is large (see Ref. [10] and the references therein). This may also explain threshold enhancements seen in several modes such as B^- → p\ov p K^- and B^- → p\ov p K^0 [11-12]. If processes with low energy release are favored, the production of low-lying charmed baryon resonances such as Ξ'_c may be substantial. There is currently no experimental evidence for the production of Ξ'_c in B decays.

2 THE BABAR DETECTOR AND DATASET

The data used in this analysis were collected with the BABAR detector at the SLAC PEP-II asymmetric energy storage ring. A total of (231.9 ± 3.5) fb^{-1} of data are used, of which 210.3 fb^{-1} were
taken on the $\Upsilon(4S)$ resonance ($\sqrt{s} = 10.58$ GeV) and the remaining 21.6 fb$^{-1}$ were taken below the $B\bar{B}$ threshold ($\sqrt{s} = 10.54$ GeV). The on-resonance data contains $(228.3 \pm 2.5) \times 10^6$ $B\bar{B}$ pairs. The BABAR detector is described elsewhere [13].

Simulated events with $\Xi_c'$ decaying into the desired final states are generated for the processes $e^+e^- \rightarrow c\bar{c} \rightarrow \Xi_c'X$ and $e^+e^- \rightarrow \Upsilon(4S) \rightarrow B\bar{B} \rightarrow \Xi_c'X$, where $X$ represents the rest of the event. The PYTHIA simulation package [14], tuned to the global BABAR data, is used for the $c\bar{c}$ fragmentation and for $B$ decays to $\Xi_c'$, and GEANT4 [15] is used to simulate the detector response.

3 ANALYSIS METHOD

3.1 Overview

The $\Xi_c'^+$ and $\Xi_c'^0$ are reconstructed through the following decays:

\[
\Xi_c'^+ \rightarrow \Xi_c'^+ \gamma \\
\Xi_c'^0 \rightarrow \Xi_c'^0 \gamma,
\]

where the daughter $\Xi_c$ baryons are reconstructed as follows:

\[
\Xi_c'^+ \rightarrow \Xi^- \pi^+ \pi^+ \\
\Xi_c'^0 \rightarrow \Xi^- \pi^+ \\
\Xi_c'^- \rightarrow \Lambda \pi^- \\
\Lambda \rightarrow p \pi^-.
\]

The measured invariant mass spectra of the $\Xi_c'$ candidates are corrected for efficiency. From the $\Xi_c'$ yields in different $p^*$ intervals, the production rates from $B$ decay and from the continuum are extracted. We also study the helicity angle ($\theta_h$) distribution.

3.2 Selection and reconstruction of $\Xi_c'^+$ and $\Xi_c'^0$

A $\Lambda$ candidate is reconstructed by identifying a proton with $dE/dx$ and Cherenkov angle measurements [13] and combining it with an oppositely charged track interpreted as a $\pi^-$, and fitting the tracks to a common vertex. The $\Lambda$ candidate is then combined with a negatively charged track interpreted as a $\pi^-$, and fitted to a common vertex to form a $\Xi^-$ candidate. For each $\Lambda$ and $\Xi^-$, the invariant mass is required to be within $3\sigma$ of the central reconstructed value, where $\sigma$ is the fitted mass resolution (approximately $1.0$ MeV/$c^2$ for $\Lambda$ and $1.5$ MeV/$c^2$ for $\Xi^-$). The invariant mass is then constrained to the nominal value [2]. Each resulting $\Xi^-$ candidate is then combined with one or two positively charged tracks interpreted as $\pi^+$ to form a $\Xi_c'^0$ or $\Xi_c'^+$ candidate. No mass constraint is applied to the $\Xi_c$ candidates.

Since the $\Xi^-$ has a long lifetime ($c\tau = 4.9$ cm), we improve the signal-to-background ratio by rejecting prompt background. The displacement vector from the event primary vertex to the $\Xi^-$ decay vertex is required to be at least 2.5 mm in the plane transverse to the beam direction. In addition, the scalar product of the displacement vector with the $\Xi^-$ momentum vector is required to be positive, rejecting unphysical candidates. These criteria were optimized in a previous analysis [7] and were finalized before the $m(\Xi_c\gamma)$ spectrum was examined in data.

The invariant mass distributions for the $\Xi_c$ candidates satisfying these criteria are shown in Fig. The fitted function (black curve) is the sum of two Gaussian functions with a common mean
for the signal plus a first-order polynomial for the background. The half-widths at half-maximum $(\sigma)$ of the signal lineshapes are 7.0 MeV/$c^2$ and 7.5 MeV/$c^2$ for $\Xi^+_c$ and $\Xi^0_c$, respectively.

3.3 Reconstruction of $\Xi^{'+}_c$ and $\Xi^{0}_c$

Clusters of energy in the electromagnetic calorimeter are identified. The cluster must spread over at least two crystals. Clusters which lie along the trajectory of a charged track in the event are eliminated. The remaining clusters define photon candidates. The energy of the photon candidate must be at least 30 MeV and the lateral moment (defined in Ref. [16]) must be less than 0.8. The $\Xi_c$ candidates shown in Fig. 1 are then combined with each of the photon candidates to form $\Xi^{'+}_c$ candidates. The mass difference $\Delta m$ is then computed:

$$\Delta m = \begin{cases} 
m(\Xi^- \pi^+ \pi^+ \gamma) - m(\Xi^- \pi^+ \pi^+) & \text{for } \Xi^{'+}_c \\
m(\Xi^- \pi^+ \gamma) - m(\Xi^- \pi^+) & \text{for } \Xi^{0}_c 
\end{cases}$$

Since $\Delta m$ and $m(\Xi^- \pi^+ [\pi^+])$ are essentially uncorrelated and the mass difference between $\Xi^{'+}_c$ and $\Xi_c$ is small, this method gives good mass resolution and avoids the need to apply a mass-constraint to the $\Xi_c$ candidates. To make the spectra easier to interpret, we plot the mass difference $\Delta m$ plus a constant offset $m_{\text{offset}}$ which is approximately equal to the nominal ground state mass; offsets of 2.467 GeV/$c^2$ and 2.471 GeV/$c^2$ are used for the $\Xi^{'+}_c$ and $\Xi^{0}_c$ states, respectively. The spectra thus obtained are shown for $\Xi^{'+}_c$ and $\Xi^{0}_c$ in Fig. 2. For each mode, the mass spectrum is shown for $p^* > 0.0$ GeV/$c$ (upper), $p^* > 2.5$ GeV/$c$ (middle), and $p^* > 3.5$ GeV/$c$ (lower). Clear $\Xi^{'+}_c$ signals are observed at a mass of approximately 2.58 GeV/$c^2$.

The photon selection criteria are quite loose, especially in comparison to the previous CLEO analysis which imposed a minimum photon energy of 100 MeV in addition to requirements on the lateral shower profile and a veto of photons from $\pi^0$ candidates. The reason for the different selection strategies is evident from a comparison of the energy spectra of photons from $\Xi^{'+}_c$ produced in the continuum, $\Xi^{'+}_c$ produced in $B$ decays, and background (Fig. 4). The CLEO study excluded $\Xi^{'+}_c$ from $B$ decays and was optimized for sensitivity to continuum production of $\Xi^{'+}_c$ where the photon energy is a powerful discriminant between signal and background, whereas the selection criteria for
Figure 2: The $\Xi_c\gamma$ invariant mass spectra, shown with the following $p^*$ requirements: 0.0 GeV/c (a,b), 2.5 GeV/c (c,d), 3.5 GeV/c (e,f). The left column shows $\Xi_c^+\gamma$ and the right column shows $\Xi_c^0\gamma$. The shaded histograms are taken from the $\Xi_c$ mass sidebands (5$\sigma$–8$\sigma$ from the central value, where $\sigma$ is the $\Xi_c$ mass resolution), and the solid points are from the $\Xi_c$ signal region (within 3$\sigma$ of the central value).
this analysis were chosen to retain $\Xi'_c$ from $B$ decays with high efficiency. For illustrative purposes, the mass spectra of $\Xi'_c$ candidates with tighter selection requirements are shown in Fig. 4.

3.4 Contributions to the invariant mass spectra

Four principal categories of events contribute to the $\Xi'_c$ candidate distributions:

1. Signal $\Xi'_c \rightarrow \Xi_c \gamma$ decays which peak in both $m(\Xi^- \pi^+ [\pi^+])$ and $\Delta m$. This is shown in Fig. 5 (a).

2. Combinatoric background which does not peak in either $m(\Xi^- \pi^+ [\pi^+])$ or $\Delta m$. This is shown in Fig. 5 (b).

3. Background where a real $\Xi_c$ is combined with an unrelated photon candidate. This peaks in $m(\Xi^- \pi^+ [\pi^+])$ but not in $\Delta m$. This is shown in Fig. 5 (c).

4. Background contribution from events where a real $\Xi'_c \rightarrow \Xi_c \gamma$ decay occurs and the correct photon is found but the $\Xi_c$ is partially mis-reconstructed. This is shown in Fig. 5 (d). This category generally does not peak in $m(\Xi^- \pi^+ [\pi^+])$ but peaks in $\Delta m$ (provided the momentum of the fake $\Xi_c$ candidate is close to the real $\Xi_c$ momentum).

Categories 2 and 3 do not peak in $\Delta m$, so we describe them with a smooth polynomial function. The $\Delta m$ distribution of the fourth category is almost indistinguishable from the signal distribution.

One further possible contribution to the mass spectrum was considered: feed-down from the decay $\Xi'_c \rightarrow \Xi_c \pi^0$ where only one of the two photons produced in the $\pi^0$ decay is used, leaving the same $\Xi_c \gamma$ final state as for a $\Xi'_c$ decay. A study of this process with a simple kinematic simulation indicates that it would produce a very broad, non-peaking structure in the $\Xi'_c$ mass spectrum, and therefore falls into the third category ($\Xi_c$ background not peaking in $\Delta m$) already discussed.
Figure 4: The $\Xi_c\gamma$ invariant mass spectra, requiring that $p^* > 2.5$ GeV/c, that the photon energy be above 200 MeV, that the shower contain at least two crystals, that the lateral moment be less than 0.6, and that the shower be well-contained (shower energy within two cells of the maximum be at least 90% of the shower energy within one cell of the maximum). Plot (a) shows $\Xi_c^+\gamma$ and plot (b) shows $\Xi_c^0\gamma$. The mass windows are narrower than for Fig. 2: the shaded histograms are taken from the $\Xi_c$ mass sidebands ($5\sigma$–$7\sigma$ from the central value) and the solid points are from the $\Xi_c$ signal region (within $2\sigma$ of the central value).

3.5 Fitting procedure

The data are divided into ten $p^*$ intervals of width 0.5 GeV/c from 0.0 to 5.0 GeV/c. For each $p^*$ interval, the $\Delta m$ distributions are fitted with the combination of a signal lineshape extracted from the simulated signal events and a second-order polynomial function to describe the background. The signal lineshape is parameterized as the sum of three Gaussian functions, parameters of which are determined from a fit to a high-statistics sample of simulated signal events in the corresponding $p^*$ range. The lineshape is described in more detail in Section A.1 of Appendix A. During this fit all nine parameters of the triple Gaussian function are allowed to vary independently within fixed ranges.

The fit to the data is performed in several steps:

1. First, we fit just the background function to an upper mass sideband of $\Xi_c^*$, $2625 < \Delta m + m_{\text{offset}} < 2900$ MeV/c$^2$, using a binned maximum likelihood method. This provides the initial values of the background parameters.

2. Next, we attempt to fit the combined background and signal functions in the mass range 2550–2700 MeV/c$^2$. The signal mass and yield are floated, with the initial value of the signal yield set to zero. The background parameters are also left free; all other parameters are fixed. The mass is initially set to a central value extracted from a fit to the entire dataset and is allowed to vary within 10 MeV/c$^2$ around this value. The fit uses a binned maximum likelihood method, followed by a binned $\chi^2$ minimization with MINOS error-handling enabled.

5 Fewer signal events were generated at the extremes of the $p^*$ spectrum. In cases where fewer than 1,000 signal events were reconstructed, only two Gaussian functions were used. This applies to 0.0–0.5 GeV/c for $\Xi_c^+$, and to 4.0–4.5 GeV/c for both $\Xi_c^+$ and $\Xi_c^0$. For 4.5–5.0 GeV/c no signal events were generated, so the fits of 4.0–4.5 GeV/c were used.
Figure 5: Illustrations of the signal and background contributions for $\Xi^0\gamma$ in simulated continuum events. Plot (a) shows category 1, correctly reconstructed signal. Plot (b) shows category 2, combinatoric background. Plot (c) shows category 3, background with real $\Xi_c$. Plot (d) shows category 4, where a photon from a real $\Xi'_c$ decay is combined with an incorrectly reconstructed $\Xi_c$. 
3. We then check whether the fit converges to a physical value. If the signal mass is within 2 MeV/c^2 of the edge of the allowed range or the yield is unphysical (above 50,000 or below −100), we reject the fit. This typically occurs when studying a region of phase space where the signal yield is too small to fit with a floating mass.

4. If the first fit is rejected, we reset the parameters to the initial values described in step 2 and fix the mass to the central value extracted from the fit to the entire dataset. The fit is then repeated.

The individual fitted spectra are shown in Appendix B.

To remove the category 4 background described in Section 3.4, we perform a sideband subtraction in \( m(\Xi^-\pi^+[\pi^+]) \) as follows:

- The \( \Delta m \) distribution of events in the \( \Xi_c \) mass signal region \(-3\sigma < m(\Xi^-\pi^+[\pi^+]) - m_0 < +3\sigma\) is plotted, where \( \sigma \) is the \( \Xi_c \) mass resolution and \( m_0 \) is the central value of the \( \Xi_c \) mass peak.
- Similarly, the \( \Delta m \) distribution for events in the \( \Xi_c \) mass sidebands, \( 5\sigma < |m(\Xi^-\pi^+[\pi^+]) - m_0| < 8\sigma \), is plotted.
- The \( \Delta m \) distributions are fitted with a signal lineshape plus a polynomial background as described above. The integral of the signal function gives the combined yields of events from categories 1 and 4 in that \( m(\Xi^-\pi^+[\pi^+]) \) range.
- The fitted yield from the sidebands is subtracted from the fitted yield in the signal region.

This process suppresses the category 4 background but retains the signal with high efficiency (∼95% at low \( p^* \) and ∼90% at high \( p^* \)). A small fraction of category 4 events have peaking structure in \( m(\Xi^-\pi^+[\pi^+]) \) and survive the sideband subtraction; this rate is 1% or less of the category 1 rate in all cases so we neglect it.

After performing the sideband subtraction described above, the numbers of background-subtracted \( \Xi'^{+} \) and \( \Xi'^{0} \) are 3341 ± 375 and 3195 ± 301, respectively. The \( p^* \) distributions are shown in Fig. 6. As discussed in Section 1, there are two contributions: \( \Xi_c' \) from B decays and from the continuum. \( \Xi_c' \) produced in B decays have low momentum, especially if the recoiling antibaryon is also charmed. Allowing for the motion of the B mesons, the kinematic limit is \( p^* < 2.08 \text{ GeV/c} \), but this corresponds to the process \( B \rightarrow \Xi'_c \pi \) which is heavily suppressed. The limit for Cabibbo-allowed processes is \( p^* < 2.02 \text{ GeV/c} \). By contrast, continuum production occurs mainly at higher values of \( p^* \), with a kinematic limit of \( p^* < 4.63 \text{ GeV/c} \) at \( \sqrt{s} = 10.6 \text{ GeV} \). Two separate peaks corresponding to these processes are clearly visible in Fig. 6.

### 3.6 Efficiency correction

For each \( p^* \) interval, the efficiency \( \varepsilon \) is determined from simulated events in the corresponding \( p^* \) range:

\[
\varepsilon = \frac{\text{Yield of true } \Xi_c' \text{ in } m(\Xi^-\pi^+[\pi^+]) \text{ signal window}}{\text{Number of generated } \Xi_c'},
\]

where the yield is obtained by fitting the \( \Delta m \) spectrum and true \( \Xi_c' \) are identified with MC generator information. An additional correction is made to take into account signal events which fall into the \( m(\Xi^-\pi^+[\pi^+]) \) sidebands and are subtracted from the yield as described in Section 3.5. This
Figure 6: Background-subtracted $\Xi_c$ momentum spectra, not corrected for efficiency. The yield in each $p^*$ interval is shown for (a) $\Xi'_c^+$ and (b) $\Xi'_c^0$.

Figure 7: Efficiency as a function of $p^*$ for (a) $\Xi'_c^+$ and (b) $\Xi'_c^0$. The factor $B(\Lambda \rightarrow p\pi^-)$ is not included.

correction, $\delta\varepsilon$, is obtained from the $m(\Xi^--\pi^+\pi^+)$ lineshape of simulated $\Xi'_c$ in the relevant $p^*$ range:

$$\delta\varepsilon = \frac{\text{Yield of true } \Xi'_c \text{ in } m(\Xi^--\pi^+\pi^+)^\text{sideband}}{\text{Yield of true } \Xi'_c \text{ in } m(\Xi^--\pi^+\pi^+)^\text{signal window}}.$$  \hspace{1cm} (2)

This is a small effect (approximately 1% for $\Xi'_c$ produced in $B$ decays and 2% for $\Xi'_c$ produced from the continuum). The overall efficiency, $\varepsilon(1-\delta\varepsilon)$, is shown in Fig. 7.

4 SYSTEMATIC STUDIES

The following systematic effects are considered. The first four are applied only to the overall normalization; the others are treated as fully uncorrelated and are applied to each $p^*$ interval separately. All uncertainties quoted are relative.

Particle identification: A systematic uncertainty of 3.5% is assigned to the efficiency of the proton identification, as in a previous analysis of the $\Xi_c$ system [7].
Tracking efficiency: To correct for a known discrepancy in tracking efficiency between data and simulation, systematic corrections of $(2.35 \pm 7.0)\%$ and $(1.55 \pm 5.6)\%$ are applied to the efficiency for reconstruction of $\Xi^+_c \rightarrow \Xi^- \pi^+ \pi^+$ and $\Xi^+_c \rightarrow \Xi^- \pi^+$, respectively.

Photon efficiency: Based on studies of photon-finding efficiency in control samples, a systematic uncertainty of 1.8\% is applied to the efficiency.

A branching fraction: The world-average branching fraction is $B(\Lambda \rightarrow p\pi^-) = (63.9 \pm 0.5)\%$. This results in a 0.8\% systematic uncertainty.

Finite simulation statistics: The statistical uncertainty in the efficiency calculation in each $p^*$ interval is applied as a systematic uncertainty to the specific data point. This is 5\% or lower in each interval.

Signal fitting procedure: The analysis is repeated with a different functional form for the signal lineshape, described in Section A.2 of Appendix A. For each $p^*$ interval, the systematic uncertainty is taken to be the difference between the efficiency-corrected yields from the two functional forms divided by $\sqrt{2}$. The value depends on the specific $p^*$ interval, but is typically around 5–10\%.

Background fitting procedure: The background shape is changed from a second-order polynomial to a fourth-order polynomial and the fit range is increased substantially. For each $p^*$ interval, the systematic uncertainty is taken to be the difference between the efficiency-corrected yields from the two methods divided by $\sqrt{2}$. This varies between $p^*$ intervals, but is typically around 5–10\%. In a few intervals with low yields it rises to 30–50\%, but is always lower than the statistical uncertainty.

Efficiency correction within a $p^*$ interval: If the simulation does not correctly model the $p^*$ distribution within a $p^*$ interval and the efficiency varies significantly across that interval, the efficiency may not be predicted correctly. This effect was studied in a previous analysis and found to be a few percent or less with the BABAR simulation. We assign a systematic uncertainty of 4\% for each $p^*$ interval.

Intermediate resonances in $\Xi^+_c \rightarrow \Xi^- \pi^+ \pi^+$: In the simulation, the $\Xi^+_c$ three-body decay is assumed to be entirely non-resonant. However, structure is observed in the Dalitz plot distributions in data. We determine the efficiency for two extreme cases: when the non-resonant contribution is 0\% ($\epsilon_{\text{res}}$) and when the non-resonant contribution is 100\% ($\epsilon_{\text{nonres}}$). The overall efficiency is then changed to $(\epsilon_{\text{res}} + \epsilon_{\text{nonres}})/2$ with a systematic uncertainty of $(|\epsilon_{\text{res}} - \epsilon_{\text{nonres}}|)/2$. This only affects the $\Xi^+_c$ mode. The effect is approximately 15\% at low $p^*$, dropping to zero at high $p^*$ as the efficiency becomes more uniform across the Dalitz plot.

Finite resolution: The reconstructed $p^*$ distribution is the true $p^*$ distribution convoluted by the resolution function. The resolution varies with $p^*$, but is typically 15–20 MeV/c, substantially smaller than the bin size (500 MeV/c). We therefore neglect this effect.

Admixture of $c\bar{c}$ and $B\bar{B}$ simulation: The angular distributions of $\Xi'_c$ produced in continuum events and in $B$ decays differ, resulting in slightly different efficiencies for the two processes. This is modelled in the simulation. In general it is unambiguous which process dominates in a given $p^*$ interval, but in the $p^*$ interval 1.5–2.0 GeV/c both may contribute significantly,
Figure 8: The efficiency-corrected, background-subtracted \( p^* \) spectrum for (a) \( \Xi^{'\circ} c \) and (b) \( \Xi^{'\circ} c \). The curve is the simulated continuum distribution described in Section 5; it is fitted to the data for \( 2.0 < p^* < 4.5 \text{ GeV/c} \) (indicated by the dashed line).

leading to a slight dependence of the efficiency-corrected yield on the assumed relative production rates. However, the absolute yield in this interval is small and other uncertainties dominate, so we neglect this effect.

After applying these systematic corrections and uncertainties, the \( p^* \) spectrum shown in Fig. 8 is obtained. The inner error bars show the statistical uncertainty (both from data and simulation), the middle error bars show the sum in quadrature of the statistical and uncorrelated systematic uncertainties, and the outer error bars (where visible) show the sum of all uncertainties in quadrature.

5 PHYSICS RESULTS

5.1 Production rates

It is clear from Fig. 8 that there is significant \( \Xi^{'\circ} c \) production both in \( B \) decays and from the \( c\bar{c} \) continuum. We separate the contributions of the two processes as follows:

- \( B \) production of \( \Xi^{'\circ} c \) for \( p^* > 2.0 \text{ GeV/c} \) is assumed to be zero.

- Continuum production of \( \Xi^{'\circ} c \) for \( p^* > 2.0 \text{ GeV/c} \) is taken to be the sum of the measured yields in each \( p^* \) interval above 2.0 GeV/c.

- The data between 2.0 GeV/c and 4.5 GeV/c are then fitted with a suitable function, described below. The function is extrapolated down to \( p^* = 0 \) and the integral over the range 0.0–2.0 GeV/c is taken as the continuum production of \( \Xi^{'\circ} c \) in that momentum range.

- The \( B \) production of \( \Xi^{'\circ} c \) below 2.0 GeV/c is taken to be the sum of the measured yields in each \( p^* \) interval below 2.0 GeV/c less the estimated continuum production in the range 0.0–2.0 GeV/c.
Figure 9: Comparison of the efficiency corrected yields in the off-peak sample with those of the full data set (off-peak and on-peak combined). The off-peak yields have been scaled up to account for the difference in integrated luminosity, and corrected for the small change in the continuum cross-section with \(\sqrt{s}\). Plot (a) shows the \(\Xi^+_c\) and plot (b) shows the \(\Xi^0_c\). Systematic uncertainties and corrections are not included.

The continuum function is based on the Bowler fragmentation model [18], tuned to the global \(\text{BaBar}\) data and implemented within the JETSET [14] generator. Only the amplitude is allowed to float in the fit to the data. The fitted function is shown in Fig. 8. The \(\chi^2/\text{NDF}\) of the fits are 1.2/4 and 1.8/4 for \(\Xi^+_c\) and \(\Xi^0_c\), respectively.

To test the model dependency, we fit the data with a number of other fragmentation models. For these crosschecks, we take the parameterizations to be functions of the scaled momentum \(x_p\). The data above 2.0 GeV/c are well-described by the Peterson model [19] and by a baryon-specific version of the phenomenological model of Kartvelishvili et al. [20]. The standard deviation of the extracted rates when using these three fragmentation models is quoted as the model-dependent uncertainty:

\[
\begin{align*}
\Xi^+_c \text{ from continuum:} & \quad 32681 \pm 5516 \text{ (exp.)} \pm 4443 \text{ (model)} \\
\Xi^+_c \text{ from } B \text{ decay:} & \quad 77199 \pm 7907 \text{ (exp.)} \pm 4443 \text{ (model)} \\
\Xi^0_c \text{ from continuum:} & \quad 16356 \pm 2509 \text{ (exp.)} \pm 1384 \text{ (model)} \\
\Xi^0_c \text{ from } B \text{ decay:} & \quad 30782 \pm 3088 \text{ (exp.)} \pm 1384 \text{ (model)},
\end{align*}
\]

where the experimental uncertainties combine both statistical and systematic effects. Excluding the normalization systematic uncertainties, these correspond to a statistical significance for \(\Xi^+_c\) production in \(B\) decays in excess of 12\(\sigma\) for each mode, and a significance for continuum production at \(p^* > 2.0\) GeV/c in excess of 6\(\sigma\) for each mode. As an additional crosscheck, the continuum production for \(p^* < 2.0\) GeV/c is measured in the off-peak data sample alone. This procedure is model-independent (to 2–3\%) but has a much larger statistical uncertainty. The results are shown in Fig. 9 and are consistent with the yields quoted above within statistical uncertainties.

Dividing the above yields by twice the total number of \(B\bar{B}\) pairs in the data sample, we measure the product branching fractions as:

\[
\begin{align*}
B(B \to \Xi^+_c X) \times B(\Xi^+_c \to \Xi^- \pi^+ \pi^+) & = [1.69 \pm 0.17 \text{ (exp.)} \pm 0.10 \text{ (model)}] \times 10^{-4} \\
B(B \to \Xi^0_c X) \times B(\Xi^0_c \to \Xi^- \pi^+) & = [0.67 \pm 0.07 \text{ (exp.)} \pm 0.03 \text{ (model)}] \times 10^{-4}.
\end{align*}
\]
Comparing the second measurement with a previous BABAR result [7],

\[ \mathcal{B}(B \rightarrow \Xi_c^0 X) \times \mathcal{B}(\Xi_c^0 \rightarrow \Xi^- \pi^+) = [2.11 \pm 0.19 \text{ (stat.)} \pm 0.25 \text{ (sys.)}] \times 10^{-4}, \]

we observe that approximately one third of \( \Xi_c^0 \) produced in \( B \) decays come from \( \Xi_c^0 \) decays.

Correcting for the \( 1/s \) scaling of the continuum cross-section for data taken at \( \sqrt{s} = 10.54 \text{ GeV} \) and taking into account the 1.5\% systematic uncertainty on the integrated luminosities quoted in Section 2, the cross-sections at \( \sqrt{s} = 10.58 \text{ GeV} \) are:

\[ \sigma(e^+e^- \rightarrow \Xi_c^0 X) \times \mathcal{B}(\Xi_c^0 \rightarrow \Xi^- \pi^+) = 141 \pm 24 \text{ (exp.)} \pm 19 \text{ (model) fb} \]
\[ \sigma(e^+e^- \rightarrow \Xi_c^0 X) \times \mathcal{B}(\Xi_c^0 \rightarrow \Xi^- \pi^+) = 70 \pm 11 \text{ (exp.)} \pm 6 \text{ (model) fb}. \]

Comparing this with a previous BABAR result [7]:

\[ \sigma(e^+e^- \rightarrow \Xi_c^0 X) \times \mathcal{B}(\Xi_c^0 \rightarrow \Xi^- \pi^+) = 388 \pm 39 \text{ (stat.)} \pm 41 \text{ (sys.) fb} \]

we observe that about 18\% of \( \Xi_c^0 \) produced in the continuum come from a \( \Xi_c^0 \).

### 5.2 Helicity angle distribution

The quark-model predicts \( J^P = \frac{1}{2}^+ \) for \( \Xi_c^0, \Xi_c^- \) and \( \Xi_c^+ \). Under this assumption, the helicity angle distribution for the decay processes studied should be flat in the cosine of the helicity angle, \( \cos \theta_h \), where \( \theta_h \) defined as is the angle between the \( \Xi^- \) direction in the \( \Xi_c \) rest frame and the \( \Xi_c \) direction in the \( \Xi_c' \) rest frame. If the \( \Xi_c' \) has \( J = \frac{3}{2} \), the angular distribution is of the form \( c_1 + c_2 \cos^2 \theta_h \) where \( c_1 \) and \( c_2 \) are unknown parameters and \( c_2 \) may be zero. In general the distribution for higher spins is a higher-order polynomial—but the distribution may be flat if the higher-order coefficients are zero. Therefore, a non-flat distribution in the data would exclude \( J = \frac{1}{2} \), but a flat distribution would not exclude \( J > \frac{1}{2} \).

The method used to measure the helicity angle distribution in the data is similar to the one used for the \( p^* \) spectrum: we divide the data into six slices of \( \cos \theta_h \) and fit the mass spectrum in each slice. A \( p^* \) threshold of 2.5 GeV/c is applied throughout to improve the signal-to-background ratio. After correcting for efficiency, the distributions are fitted with two functions: first, a flat distribution:

\[ f_0(\cos \theta_h) = \alpha \quad (3) \]

and second, a symmetric quadratic:

\[ f_0(\cos \theta_h) = \alpha \left( 1 + \beta \cos^2 \theta_h \right). \quad (4) \]

Separate fits to each mode in the data are performed and the fit results are shown in Table 1. The data are clearly consistent with being flat (\( \chi^2/\text{NDF} \) less than unity). The fitted quadratic parameters \( \beta \) are consistent with zero, though with large statistical uncertainties. Since the two modes should have identical helicity distributions, we weight them according to their statistical precision and combine them—this is shown in Fig. 10 and the fit results are given in Table 1. The data are still fit well by a flat distribution, though with a somewhat reduced \( \chi^2 \) probability (20\%). From this we conclude that the data are consistent with the predicted \( J = \frac{1}{2} \) but that higher spins cannot be excluded.
Figure 10: Fits to efficiency-corrected helicity distributions for data with $p^* > 2.5$ GeV/c. The plot shows the normalized, weighted sum of the $\Xi_c^{'+}$ and $\Xi_c^0$ distributions. The solid line assumes a flat helicity distribution, whereas for the dashed line a quadratic term is added.

Table 1: Results of fits to efficiency-corrected helicity distributions. The $\chi^2$ goodness-of-fit and the number of degrees of freedom are given for the flat and quadratic distributions given in Eq. 3 and 4, along with the fitted parameter $\beta$ from the quadratic distribution. The results are given for the $\Xi_c^{'+}$ and $\Xi_c^0$ samples individually, and for a weighted sum of the two samples.

|                 | $\Xi_c^{'+}$ | $\Xi_c^0$ | Weighted Sum |
|----------------|--------------|------------|--------------|
| $\chi^2$/NDF for flat | 4.0/5 (55%)  | 4.4/5 (50%) | 7.3/5 (20%)  |
| $\chi^2$/NDF for quadratic | 2.7/4 (61%)  | 1.3/4 (87%) | 3.0/4 (55%)  |
| $\beta$ for quadratic    | 0.63 ± 0.68  | 1.04 ± 0.82 | 0.79 ± 0.52  |
We have confirmed the CLEO observation of the $\Xi_c^{'+}$ and $\Xi_c^{0}$ states from the $c\bar{c}$ continuum. In addition, we found that $B$ mesons decay at a substantial rate to $\Xi_c^{'+}$ and $\Xi_c^{0}$. This is the first observation of such decays; the statistical significance is in excess of 12$\sigma$ for each mode. We have measured the production rates of $\Xi_c'$ from $B$ decays (expressed as a branching fraction) and from the $c\bar{c}$ continuum (expressed as a cross-section); in both cases, the absolute rate is scaled by the unknown absolute $\Xi_c$ branching fraction. We have measured the angular distribution of $\Xi_c' \to \Xi_c \gamma$ decays and found it to be consistent with the prediction for $J^P = \frac{1}{2}^+$. However, higher spins cannot be ruled out.

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Appendix

A Lineshape parameterizations

A.1 Triple Gaussian function

The lineshape function \( f(\Delta m) \) is parameterized as follows:

\[
f(\Delta m) = N(1 - f_2 - f_3)G(\Delta m; \mu_1, \sigma_1) + N f_2 G(\Delta m; \mu_1 + \Delta \mu_2, \sigma_2) + N f_3 G(\Delta m; \mu_1 + \Delta \mu_3, \sigma_3)
\]

where \( G(x; \mu, \sigma) \) is a Gaussian function of unit area with mean \( \mu \) and width \( \sigma \). The nine parameters are then interpreted as follows:

- \( N \) Total fitted yield
- \( f_2 \) Fraction of yield in second Gaussian function
- \( f_3 \) Fraction of yield in third Gaussian function
- \( \mu_1 \) Signal mass
- \( \Delta \mu_2 \) Mean of second Gaussian function with respect to the signal mass
- \( \Delta \mu_3 \) Mean of third Gaussian function with respect to the signal mass
- \( \sigma_1 \) Width of first Gaussian function
- \( \sigma_2 \) Width of second Gaussian function
- \( \sigma_3 \) Width of third Gaussian function

When fitting simulated events to determine the lineshape, all nine parameters are allowed to vary independently. In order to improve fit convergence, the following bounds are placed on the variation of the parameters:

- \( N \) No bounds
- \( f_2 \) No bounds
- \( f_3 \) No bounds
- \( \mu_1 \) Limited to \((-5, +5) \) MeV/c\(^2\) relative to the true mass
- \( \Delta \mu_2 \) Limited to \((-15, +5) \) MeV/c\(^2\) relative to \( \mu_1 \)
- \( \Delta \mu_3 \) Limited to \((-35, -5) \) MeV/c\(^2\) relative to \( \mu_1 \)
- \( \sigma_1 \) Limited to \((0, 10) \) MeV/c\(^2\)
- \( \sigma_2 \) Limited to \((4, 20) \) MeV/c\(^2\)
- \( \sigma_3 \) Limited to \((20, 100) \) MeV/c\(^2\)

A.2 Alternative lineshape parameterization

The following functional form was also used as a cross-check and to determine the systematic uncertainty due to the signal lineshape:

\[
f(x) = A_p \times \begin{cases} \exp \left[ \frac{4\xi \sqrt{\xi^2 + 1} (x-x_1) \ln 2}{h_p \left( \sqrt{\xi^2 + 1} - \xi \right) \ln \left( \sqrt{\xi^2 + 1} + \xi \right)} + \rho_1 \cdot \left( \frac{x-x_1}{x_p-x_1} \right)^2 - \ln 2 \right] & , x < x_1, \\ \exp \left[ -2 \cdot \left( \frac{\ln 1 + 4\xi \sqrt{\xi^2 + 1} (x-x_1) \ln 2}{\ln 1 + 2\xi^2 - 2\xi \sqrt{\xi^2 + 1}} \right)^2 \right] & , x_1 < x < x_2, \\ \exp \left[ -\frac{4\xi \sqrt{\xi^2 + 1} (x-x_2) \ln 2}{h_p \left( \sqrt{\xi^2 + 1} - \xi \right) \ln \left( \sqrt{\xi^2 + 1} + \xi \right)} + \rho_2 \cdot \left( \frac{x-x_2}{x_p-x_2} \right)^2 - \ln 2 \right] & , x > x_2. \end{cases}
\]
where

\[ x_1 \equiv x_p + \frac{h_p}{2} \left[ \frac{\xi}{\sqrt{\xi^2 + 1}} - 1 \right] \]

\[ x_2 \equiv x_p + \frac{h_p}{2} \left[ \frac{\xi}{\sqrt{\xi^2 + 1}} + 1 \right] . \]

Of the six parameters \( A_p \) controls the amplitude, \( x_p \) controls the peak position, \( h_p \) controls the width, \( \xi \) controls the asymmetry in the central region, \( \rho_1 \) controls the lower tail, and \( \rho_2 \) controls the upper tail.

**B Individual mass spectra**

The fitted mass spectra for individual \( p^* \) intervals are shown in Fig. 11 and 12 for \( \Xi_0' c \) and \( \Xi_0 c \), respectively.
Figure 11: The $\Xi_c^+\gamma$ invariant mass spectra for each of the ten $p^*$ intervals used. The points show data from the $\Xi_c^+$ signal mass region (within 3$\sigma$ of the central value).
Figure 12: The $\Xi^0_c\gamma$ invariant mass spectra for each of the ten $p^*$ intervals used. The points show data from the $\Xi^0_c$ signal mass region (within 3$\sigma$ of the central value).