ABSTRACT
Using 1 cm and 3 mm CARMA and 2 mm GISMO observations, we follow up the first extragalactic detection of anomalous microwave emission (AME) reported by Murphy et al. (2010) in an extranuclear region (Enuc. 4) of the nearby face-on spiral galaxy NGC 6946. We find the spectral shape and peak frequency of AME in this region to be consistent with models of spinning dust emission. However, the strength of the emission far exceeds the Galactic AME emissivity given the abundance of polycyclic aromatic hydrocarbons (PAHs) in that region. Using our galaxy-wide 1 cm map (21″ resolution), we identify a total of eight 21″ x 21″ regions in NGC 6946 that harbour AME at > 95% significance at levels comparable to that observed in Enuc. 4. The remainder of the galaxy has 1 cm emission consistent with or below the observed Galactic AME emissivity per PAH surface density. We probe relationships between the detected AME and dust surface density, PAH emission, and radiation field, though no environmental property emerges to delineate regions with strong versus weak or non-existent AME. We argue that the spinning dust hypothesis, which predicts the AME power to be approximately proportional to the PAH mass, is therefore incomplete.

Key words: ISM: dust – radio continuum: ISM

1 INTRODUCTION
Anomalous Microwave Emission (AME) is dust-correlated emission observed between ~ 20 – 50 GHz that cannot be accounted for by extrapolating the thermal dust emission to low frequencies. First detected as an emission excess in the microwave (Kogut et al. 1996; de Oliveira-Costa et al. 1997; Leitch et al. 1997), AME is now thought to arise from charged small grains with size ~ 3.5 – 10 Å that spin rapidly due to the action of systematic torques in the interstellar medium (Draine & Lazarian [1998]; Hoang et al. 2011; Ysard & Verstraete 2011; Silsbee et al. 2011). Subsequent Galactic observations have been well-fit with the inclusion of a spinning dust component (e.g. Miville-Deschenes et al. 2008; Planck Collaboration et al. 2011b).

Murphy et al. (2010) reported the first extragalactic detection of AME near the star-forming extra-nuclear region of the spiral galaxy NGC 6946 (hereafter Enuc. 4). NGC 6946, located at a distance of 6.8 Mpc (Karachentsev et al. 2000), is known for its intense star formation, having hosted at least nine supernovae in the last century (Prieto et al. 2008) and having a star formation rate (SFR) of 7.1 M⊙ yr⁻¹ (Kennicutt et al. 2011). Follow-up observations of Enuc. 4 by the Arcminute Microkelvin Imager (AMI) support the presence of an AME component in this source (Scaife et al. 2011).

To date, additional extragalactic detections have proven elusive. Planck observations of the Small Magellanic Cloud (SMC) have shown evidence for an AME component (Planck Collaboration et al. 2011c; Draine & Hensley 2012), but the interpretation is complicated by additional excess emission possibly arising from the large grains. Despite microwave observations of other dusty, star-forming galaxies including Andromeda, only upper limits on an AME component have been placed (Peel et al. 2011; Ade et al. 2014). The difficulty in finding extragalactic AME has hindered our ability to probe variations of AME properties.
within a galaxy, particularly identifying the hallmarks of regions with strong emission. In this work, we use high resolution data from the Combined Array for Research in Millimeter-wave Astronomy (CARMA) at 3 mm to better constrain the spectral energy distribution (SED) of Enuc. 4. We combine these CARMA observations with data from Spitzer, Herschel, the Goddard IRAM Superconducting 2 Millimeter Observer (GISMO), the Very Large Array (VLA), and the Westerbork Synthesis Radio Telescope (WSRT) to create composite SEDs that allow us to decompose the emission into components from thermal dust, synchrotron, free-free, and AME. We compare the AME found in Enuc. 4 to that observed in the Galaxy and assess the viability of the spinning dust mechanism for explaining the emission.

The CARMA 1 cm map provides coverage of the whole galaxy, enabling a search for AME beyond Enuc. 4. As we find multiple additional regions with AME, we use the high-resolution dust model fitting of NGC 6946 by Aniano et al. (2012) to explore correlations between the AME and local properties such as dust surface density, PAH emission, and the intensity of the local radiation field.

We have organised the paper as follows: in Section 2 we describe the data used in this analysis and our data reduction; in Section 3 we perform fits to the SEDs using models for emission from thermal dust, free-free, synchrotron, and AME and analyse the results of the fits for particular regions of the Galaxy; in Section 4 we analyse galaxy-wide correlations between AME and local galaxy properties and comment on the nature of the AME observed in NGC 6946 versus Galactic observations; in Section 5 we discuss the implications of our observations for spinning dust theory; and in Section 6 we summarise our conclusions.

2 DATA REDUCTION AND SED SYNTHESIS

In this Section we describe the datasets used in our analysis. The properties of all maps are summarised in Table 1.

2.1 CARMA Data

CARMA consists of 23 antennas– six 10 m, nine 6 m, and eight 3.5 m. The CARMA 3 mm data were taken with 6 and 10 m antennas in the CARMA E configuration with baseline lengths between 8.5 and 66 m in July 2010. The map has a resolution of 9.1′ and an rms noise level of 0.017 mJy/beam. The CARMA 1 cm data were taken with 6 and 8.5 m Sunyaev-Zel’dovich Array antennas in October 2010 and July 2011 using both the SH and SL configurations. The map has a resolution of 18.8′ and an rms noise level of 0.017 mJy/beam. The CARMA 1 cm map provides coverage of the whole galaxy, enabling a search for AME beyond Enuc. 4. As we find multiple additional regions with AME, we use the high-resolution dust model fitting of NGC 6946 by Aniano et al. (2012) to explore correlations between the AME and local properties such as dust surface density, PAH emission, and the intensity of the local radiation field.

2.2 GISMO Data

GISMO is a Transition Edge Sensor bolometer camera on the IRAM 30 m telescope that operates in the 2 mm atmospheric window (Staguhn et al. 2003, 2014). A total of 1.5 hours of integration time was obtained on Enuc. 4 in April 2013 at 17′ resolution. The data were reduced using the CRUSH software package “deep mode” (Kovács 2008), which includes large-scale filtering to mitigate atmospheric effects.

2.3 Ancillary Data

2.3.1 IR Data

NGC 6946 was part of both the Spitzer Infrared Nearby Galaxies Survey (SINGS) (Kennicutt et al. 2003) and Key Insights on Nearby Galaxies: a Far-Infrared Survey with Herschel (KINGFISH) (Kennicutt et al. 2011) projects, and thus has extensive Spitzer and Herschel observations. We use the same dataset detailed in Aniano et al. (2012) consisting of 3.6, 4.5, 5.8, and 8.0 μm IRAC images and 24 and 70 μm MIPS images from SINGS, and 70, 100, and 160 μm PACS images and a 250 μm SPIRE image from KINGFISH. We do not use the 160 μm MIPS image or the SPIRE 350 or 500 μm images due to insufficient angular resolution. All of the remaining images have resolution better than our 18.8′ CARMA 1 cm map.

2.3.2 Radio Data

We employ the same radio data as Murphy et al. (2010). These consist of the 1.4 GHz radio map from the WSRT-SINGS survey (Braun et al. 2007) with a 14′ x 12.5′ beam and VLA maps at 1.5, 1.7, 4.9, and 8.5 GHz, all with 15′ x 15′ beams (Beck 2007).

2.4 SED Synthesis

We combined all data by convolving each image with a Gaussian kernel to a common 21′ resolution (Aniano et al. 2011). This corresponds to a physical scale of about 700 pc at the distance of NGC 6946.

3 ENUC. 4

The new observations at 1 cm and 3 and 2 mm allow us to revisit the SED of Enuc. 4 obtained by Murphy et al. (2010) and place tighter constraints on the frequency-dependence of the AME. In particular, the inclusion of the 2 and 3 mm data allow us to better constrain the sum of the AME and thermal dust contributions and verify the presence of a spectral peak in the 30 GHz range. We extract the flux density in a 21′ diameter circular aperture centred on the Enuc. 4 position given by Murphy et al. (2010).

3.1 Fits Without Spinning Dust

We first attempt to fit the Enuc. 4 SED without invoking a spinning dust component. We model the synchrotron emission as a power law with unknown normalisation and index, i.e.

\[ F_\nu^{\text{sync}} = A \left( \frac{\nu}{1.36 \text{ GHz}} \right)^{-\alpha_{\text{sync}}} \]  

(1)

where \( A \) is the normalisation, \( \nu \) is the frequency, and \( \alpha_{\text{sync}} \) is the index of the synchrotron spectral energy distribution. The data were fitted with MIRIAD. We find multiple additional regions with AME, we use the high-resolution dust model fitting of NGC 6946 by Aniano et al. (2012) to explore correlations between the AME and local properties such as dust surface density, PAH emission, and the intensity of the local radiation field.
Characterizing Extragalactic Anomalous Microwave Emission in NGC 6946 with CARMA

Figure 1. Left: We overlay the emission contours from the 1 cm map on the IRAC 8 μm image, where the ten contour levels are linearly spaced between the 3 σ noise level of 0.048 MJy/sr and 0.48 MJy/sr. The eight pixels with significant AME detections are shown in black boxes with numbering corresponding to Table 1. Right: We overlay the emission contours from the 2 mm (green solid) and 3 mm (cyan dashed) maps on the 1 cm image in the Enuc. 4 region (indicated by the solid rectangle in the left panel), demonstrating excellent coincidence of the emission in all three maps. The five 2 mm contours are linearly spaced between 0.05 and 0.2 MJy/sr while the five 3 mm contours are linearly spaced between 0.04 and 0.13 MJy/sr.

Table 1. Data Summary

| Instrument | λ (μm) | FWHM ″ | σRMS (MJy/sr) | σCalibration (%) | Reference |
|------------|--------|---------|---------------|-----------------|-----------|
| IRAC 3.6   | 3.6    | 1.90    | 0.0093        | 5               | Aniano et al. (2012) |
| IRAC 4.5   | 4.5    | 1.81    | 0.0093        | 5               | Aniano et al. (2012) |
| IRAC 5.8   | 5.8    | 2.11    | 0.0274        | 5               | Aniano et al. (2012) |
| IRAC 8.0   | 8.0    | 2.82    | 0.0356        | 5               | Aniano et al. (2012) |
| MIPS 24    | 24     | 6.43    | 0.0328        | 5               | Aniano et al. (2012) |
| MIPS 70    | 70     | 18.7    | 0.334         | 10              | Aniano et al. (2012) |
| PACS 70    | 70     | 5.67    | 2.52          | 10              | Aniano et al. (2012) |
| PACS 100   | 100    | 7.04    | 2.22          | 10              | Aniano et al. (2012) |
| PACS 160   | 160    | 11.2    | 1.53          | 20              | Aniano et al. (2012) |
| SPIRE 250  | 250    | 18.2    | 0.873         | 15              | Aniano et al. (2012) |
| GISMO      | 2000   | 21.0    | 0.060         | 10              | This work |
| CARMA 3000 | 3000   | 9.1     | 0.017         | 10              | This work |
| CARMA 10000| 10000  | 18.8    | 0.016         | 10              | This work |
| VLA 30000  | 30000  | 14      | 0.010         | 5               | Braun et al. (2007) |
| VLA 60000  | 60000  | 14      | 0.011         | 5               | Braun et al. (2007) |
| VLA 18000  | 18000  | 14      | 0.006         | 5               | Braun et al. (2007) |
| VLA 20000  | 20000  | 14      | 0.006         | 5               | Braun et al. (2007) |
| WSRT 22000 | 22000  | 15      | 0.004         | 5               | Beck (2007) |

We adopt two fitting strategies for the synchrotron slope. Guided by the results of Niklas et al. (1997), in the first approach we put a Gaussian prior with mean 0.83 and standard deviation 0.13 on $\alpha_{\text{sync}}$. This is a safeguard against fits that yield unphysically low values of $\alpha_{\text{sync}}$ to compensate enhanced 1 cm emission. In the second, we simply draw values for $\alpha_{\text{sync}}$ uniformly between 0.5 and 1.5. Our results are robust to this choice, and thus we adopt the latter as the default for its simplicity. To fit the amplitude, we expect that the synchrotron comprises the majority of the emission at 22 cm and therefore draw the synchrotron normalisation $A$ uniformly between 0 and the 5σ upper-limit on the 22 cm data point.

It is unclear whether a power law is a good description of the synchrotron emission over the frequency range of interest. In particular, the Galactic synchrotron index has been observed to steepen by $\sim 0.3$ between 13 and 1 cm in analyses of WMAP and Planck data (e.g. Bennett et al. 2003; Planck Collaboration et al. 2014a). Such steepening is expected when electrons with requisite energy are no longer able to be produced. Our data have insufficient frequency sampling to meaningfully constrain a break frequency or the
resulting index. Therefore, we consider the extreme case in which the synchrotron produces no emission below 3 cm. Although this will not substantially affect the modeling of the emission in Enc. 4, steepening is required to explain the SED of other regions of the galaxy, as discussed in detail in Section 3.

We model the free-free emission as a power law with fixed index -0.12 and unknown normalisation, i.e.

$$F^\text{ff}_{\nu} = B \left( \frac{\nu}{30 \text{ GHz}} \right)^{-0.12} .$$  \hspace{1cm} (2)

Because we possess the full infrared SED of the galaxy, we can constrain the free-free emission based on the empirical relations from Murphy et al. (2012) connecting the thermal emission, 24 µm flux density, and total IR luminosity to the star formation rate. Combining their Equations 6 and 14 and assuming an electron temperature of $10^4$ K, we obtain

$$F^\text{ff}_{\nu, 1 \text{ cm}} = 4.74 \times 10^{-3} F_{\nu, 24 \mu\text{m}} . \hspace{1cm} (3)$$

Likewise, combining their Equations 6 and 15, we obtain

$$\left( \nu L_{\nu} \right)_{1 \text{ cm}}^\text{ff} = 1.46 \times 10^{-6} L_{\text{IR}} . \hspace{1cm} (4)$$

The total IR luminosity from dust has been estimated for each pixel by Aniano et al. (2012) (their Equations 14 and 21) by fitting the infrared SED with the Draine & Li (2007) dust model, and we use this value as $L_{\text{IR}}$ here.

We adopt two approaches to fit the free-free. In the first, we draw $B$ uniformly between half the minimum and twice the maximum values computed with Equations 3 and 6 which would accommodate both variations in electron temperature and intrinsic scatter in the relations of Murphy et al. (2011, 2012). In the second, we draw uniformly between 0 and the $5\sigma$ upper limit on the 1 cm emission. We find that our results are robust to choice of prior and adopt the latter method as the default for its simplicity.

Enc. 4 has a 24 µm flux density of $5.1 \times 10^{-2}$ Jy, implying $2.4 \times 10^{-4}$ Jy of free-free emission at 1 cm. We note immediately that this is far below the total observed 1 cm flux density of $1.3 \times 10^{-3}$ Jy.

For the thermal dust component, we assume a power law of the form

$$F_{\nu} = C \left( \frac{\nu}{150 \text{ GHz}} \right)^{\beta} ,$$  \hspace{1cm} (5)

where we fix $\beta = 3.65$ in accord with measurements of the thermal dust SED by Planck and draw $C$ uniformly between 0 and the $5\sigma$ upper limit on the 2 mm (150 GHz) data point.

To perform the fit, we make $2 \times 10^5$ draws from the prescribed distribution for each parameter, then compute the likelihood $L$ of each model explicitly:

$$L \propto \prod_i e^{-\frac{(\hat{F}_i - F_i)^2}{2\sigma_i^2}} , \hspace{1cm} (6)$$

where the $\hat{F}_i$ is the flux density estimated by the model at frequency $i$ and $F_i$ is the data at frequency $i$ that has error $\sigma_i$. The proportionality constant has been omitted since we compare only the relative likelihood of models. We find the 1D confidence intervals for each parameter by marginalising over the others. We obtain nearly identical results on repeating this process, indicating that the number of draws is sufficiently high to sample to the parameter space.

Figure 2b gives the fit of these three components to the data, which is poor. Additionally, the required free-free emission at 1 cm is $7.6 \times 10^{-4}$ Jy, a factor of three above the estimate based on $F_{\nu, 24 \mu\text{m}}$.

### 3.2 Spinning Dust Fits

We perform a second fit employing an additional component from spinning dust emission. Spinning dust emission is a complicated process that depends upon the size, shape, and charge of the emitting grains as well as the environmental conditions such as gas temperature, molecular fraction, ionisation state, and the intensity of the radiation field. Fitting a model that varies all of these parameters is well beyond the capabilities of the data, thus we seek instead a simple prescription for the emission. Following Draine & Hensley (2012), we parametrise the spinning dust emission as

$$F^\text{sd}_{\nu} = D \left( \frac{\nu}{v_0} \right)^2 \exp \left[ 1 - \left( \frac{\nu}{v_0} \right)^2 \right] , \hspace{1cm} (7)$$

where the peak frequency $v_0$ and the amplitude $D$ are free parameters. We restrict $v_0$ to be between 10 and 70 GHz and $D$ to be between 0 and the $5\sigma$ upper limit on the 1 cm data point. Although the model is a simplification of the underlying physics, it is nevertheless instructive to compare both the amplitude and peak frequency obtained from the fits to those of similar studies performed in the Galaxy.

Using the formalism outlined above, we obtain $D = 0.76 \pm 0.23$ mJy and $v_0 = 44 \pm 6$ GHz, corresponding to a 30 GHz flux density of 0.61 mJy. The free-free flux density at 1 cm is $5.1 \times 10^{-4}$ Jy, a factor of two above the estimate from $F_{\nu, 24 \mu\text{m}}$ but less than what was required by the fit with no spinning dust emission. Figure 2b presents the much-improved fit using this model. To quantify the improvement, we perform the likelihood ratio test by constructing the test statistic $D$:

$$D = -2 \ln \mathcal{L}_1 + 2 \ln \mathcal{L}_2 , \hspace{1cm} (8)$$

where $\mathcal{L}_1$ and $\mathcal{L}_2$ are the likelihoods of the best fit models without and with a spinning dust component, respectively. $D$ follows a $\chi^2$ distribution with the number of degrees of freedom equal to the difference in the number of free parameters in the two models, here two. We obtain $D = 13.8$, disfavouring the model with no spinning dust emission with $p \approx 10^{-3}$.

### 3.3 Thermal Dust Fits

Having fit the radio data, we now perform a more realistic modeling of the thermal dust emission. We follow the fitting strategy of Aniano et al. (2012) and employ the Draine & Li (2007) dust model. This model includes populations of silicate and carbonaceous grains, including a PAH population, heated by a distribution of radiation field intensities such
that the differential dust mass \( dM_d \) heated by starlight intensities between \( U \) and \( U + dU \) is given by

\[
\frac{1}{M_d} \frac{dM_d}{dU} = (1 - \gamma) \delta(U - U_{\text{min}}) + \gamma \frac{\alpha - 1}{U_{\text{max}} - U_{\text{min}}} U^{-\alpha}
\]

for \( U_{\text{min}} < U < U_{\text{max}} \). The heating spectrum is assumed to be the interstellar radiation field determined by Mathis et al. (1983) scaled by a constant factor \( U, U_{\text{min}}, U_{\text{max}}, \gamma, \) and \( \alpha \), are free parameters of the model to be fit. The PAH emission features require the addition of the parameter \( q_{\text{PAH}} \) defined as the total mass fraction of the dust in PAHs. Following Aniano et al. (2012), we set \( U_{\text{max}} = 10^7 \) since most pixels in NGC 6946 were best fit by this value and the model is in general relatively insensitive to the value of this parameter (Draine et al. 2007). We define \( \bar{U} \) as the dust mass-weighted mean starlight intensity heating the dust.

We fit this model to the Enuc. 4 SED 3 mm and shortward after subtracting the best fit synchrotron, free-free, and synchrotron as determined in Section 4.2. The thermal dust fit presented in Figure 3 has fit parameters \( q_{\text{PAH}} = 0.028, M_d = 1.3 \times 10^5 \, M_\odot, U_{\text{min}} = 3, \alpha = 1.7, \) and \( \gamma = 1.1 \times 10^{-3} \). \( F_{\nu}^{\text{dd}} \), the fraction of the dust luminosity radiated from regions with \( U > 100 \), has a value of 0.18.

### 3.4 Comparisons to Spinning Dust Models

For reasonable assumptions about the size distribution and electric dipole moments of small grains, Draine & Lazarian (1998a,b) calculated a spinning dust emissivity at 30 GHz of 1 × 10^{-17} Jy sr^{-1} cm^{-2} H^{-1}, consistent with the observations of Kogut et al. (1996), de Oliveira-Costa et al. (1997), and Leitch et al. (1997), though the scatter was large. Subsequent observations of the Ho-correlated AME (Dobler et al. 2009), the Perseus molecular cloud (Tibbs et al. 2010, 2011), an ensemble of Galactic clouds (Planck Collaboration et al. 2014), and the average diffuse ISM (Planck Collaboration et al. 2014) have all suggested a lower emissivity of about 3 × 10^{-18} Jy sr^{-1} cm^{-2} H^{-1}. We adopt this as our benchmark value.

Since spinning dust emission arises from the smallest grains (believed to be PAHs), its flux density should be directly proportional to the mass of small grains present, i.e. \( M_{\text{PAH}} \equiv q_{\text{PAH}} M_d \). It is therefore more appropriate to normalise the AME by PAH mass rather than by hydrogen column. Using the Galactic values of \( q_{\text{PAH}} = 0.046 \) and \( M_d/M_\odot = 0.01 \) (Draine & Li 2007), a spinning dust emissivity of 3 × 10^{-18} Jy sr^{-1} cm^{-2} H^{-1}, and taking the distance to NGC 6946 to be 6.8 Mpc (Karachentsev et al. 2000), we obtain:

\[
F_{\nu}^{\text{sd}} = 2 \times 10^{-8} \frac{M_{\text{PAH}}}{M_\odot} \, \text{Jy}
\]

From the values of \( q_{\text{PAH}} \) and \( M_d \) that were derived from fitting the thermal dust emission, Equation 10 implies \( F_{\nu}^{\text{sd}} \) = 0.06 mJy of spinning dust emission in Enuc. 4. This is more than a factor of ten below the fit value of 0.61 mJy. The emissivity observed in Enuc. 4 corresponds to 2 × 10^{-7} Jy/M_{\text{PAH}}.

Theoretical models of spinning dust emission predict that the peak frequency is sensitive to the environment, in particular the gas density. The peak frequency derived here agrees well with models of the Cold Neutral Medium (CNM) and Warm Ionized Medium (WIM) presented by Draine & Lazarian (1998a,b), but disfavor the low frequency
(≃ 20 GHz) peak predicted by models of spinning emission arising from the Warm Neutral Medium (WNM).

Other large-scale determinations of the AME peak frequency have also yielded results around 40 GHz. The all-sky AME SED extracted from WMAP [Miville-Deschênes et al. 2008] was fit in part using a CNM component peaking at ≃ 40 GHz by [Hoang et al. 2011] and [Ysard et al. 2010]. However, both models also required a dominant WNM component peaking at ≃23 GHz that we do not see here. Additionally, Ho-correlated AME was found to peak around 40 GHz [Dobler et al. 2009], consistent with spinning dust in the WIM. Stepping outside the Galaxy, the millimeter SMC SED is well-fit using a spinning dust contribution peaking at 40 GHz [Draine & Hensley 2012].

We thus conclude that the AME detected in Enuc. 4 has a spectral shape and peak frequency consistent with spinning dust emission from the CNM or WIM as seen in both the Galaxy and the SMC, but is far stronger than Galactic AME per unit PAH mass. It is possible that the dust in NGC 6946 is substantially different than Galactic dust in composition, leading to an increased spinning dust emissivity. To better understand the evolution of AME strength with environment, we investigate other regions in NGC 6946 with detected AME in the following Section.

4 GALAXY-WIDE ANALYSIS

Though centered on Enuc. 4, our CARMA 1 cm map provides coverage over the entire galaxy. We can therefore leverage the dust fitting by Aniano et al. [2012] to determine whether correlations exist between the fit AME emissivity and the dust properties of that location. To our knowledge, this is the first time such an analysis has been conducted over such a large scale in an external galaxy.

4.1 Model Fitting

We first regridded the maps at each frequency to 21′′x21′′ square pixels in order to minimise pixel-to-pixel correlations. The 2 and 3 mm maps were not used in this analysis as they cover only the region of the galaxy immediately surrounding Enuc. 4. To ensure that we are fitting galaxy and not background pixels, we require a 3σ detection in all IR and radio bands except the 1 cm band, where it is useful to place upper limits on the AME contribution. We note that using a 5σ threshold does not substantially affect the results, but does reduce the number of pixels considered.

Before performing a fit to the radio SED, we consider the 1 cm map alone. In Figure 4a, we present the histogram of 1 cm flux densities normalised by the 1σ error for the 382 pixels meeting the 3σ criterion. 44 of the pixels have detected 1 cm emission in excess of 3σ, but most pixels are consistent with the estimated noise level.

Using Equations 3 and 4 we can determine the expected free-free flux density in each of these pixels from both the 24 µm emission and \( L_{IR} \). We plot histograms of the 1 cm emission with the estimated free-free contribution subtracted in Figure 4b, where it is clear that our estimate based on \( L_{IR} \) systematically overestimates the free-free emission while the estimate based on the 24 µm emission is generally consistent with the data. This is not unexpected as the total IR luminosity will also have a contribution from dust heated by an older stellar population not associated with free-free emission around HII regions. The pixels with excess emission after subtraction could have a significant AME contribution or particularly strong free-free or synchrotron emission. SED fitting is required to discriminate between these alternatives.

We estimate the spinning dust emission in each pixel using Equation 10 and for illustration also estimate the emission using a spinning dust emissivity of \[ 2 \times 10^{-7} \text{ Jy/PAH} \] implied by our fits to Enuc. 4. We present the histogram of AME-subtracted pixels for both emissivities in Figure 4c. It is clear that the ensemble of pixels are consistent with the spinning dust emission estimated by Equation 10 but the Enuc. 4 emissivity severely overestimates the emission in most pixels even before subtracting a free-free component. In Figure 4d, we subtract both an estimate of the free-free based on \( F_{ν,24\mu m} \) (Equation 3) and an estimate of the spinning dust emission based on Equation 10. Although agreement is overall good, the histogram is skewed negative, suggesting either the free-free, AME, or both have been overestimated. Additionally, outliers with residuals in excess of 3σ remain. This could imply either a strong AME component (similar to what is observed in Enuc. 4), regions in which our free-free estimate breaks down, or regions of particularly strong synchrotron emission.

To test whether the inclusion of an AME component is warranted by the data, we fit a model with only synchrotron and free-free emission to the SED of each pixel using the likelihood method described above. The 1 cm residuals from this fit are presented in Figure 4e, illustrating that the majority of pixels have a residual at 1 cm consistent with zero, i.e. an AME component is not needed to account for the 1 cm emission in these regions. We note, however, that the histogram of residuals is skewed negative, suggesting that the radio model is overestimating the 1 cm emission even before the inclusion of an AME component.

This tension can be alleviated somewhat if the synchrotron power law steepens between 3 and 1 cm. In Figures 4f and 4g, we consider the most extreme case in which the synchrotron component drops to zero below 3 cm. That the fits continue to overestimate the 1 cm emission even in this case either suggests that the emission components are not being properly modeled at over wavelengths (particularly 3 and 6 cm) or that there is a calibration offset between the 1 cm data and some or all of the remaining points on the SED.

Given the uncertainty in the radio model, we cannot quantify precisely the AME in each pixel. However, as illustrated by Figure 4f, an emissivity per PAH mass consistent with that observed in Enuc. 4 is already ruled out from the 1 cm map alone. We can also constrain the AME in pixels with a subdominant radio component where the estimates of AME contribution are relatively insensitive to the synchrotron model, and we focus on these regions in the remainder of this Section.

While the residuals plotted in Figure 4a are helpful for identifying regions in which the free-free and synchrotron models are unable to produce enough emission at 1 cm to agree with observations, a residual fit will underestimate any true AME at 1 cm since other parts of the fit will be strained to accommodate a high 1 cm point. Thus, we perform two
additional fits. First, we fit explicitly allowing a contribution from AME at 1 cm that may be either positive or negative. Second, we fit the data 3 cm and longward with a radio model and estimate the AME as the fit residual at 1 cm. The agreement between these two methods is excellent.

Using a non-breaking synchrotron model, we identify three pixels having AME inconsistent with zero at 3σ and five additional pixels with AME significant at 2σ. If we allow no synchrotron contribution at 1 cm, we find two additional pixels significant at 2σ. The detections and their coordinates are listed in Table 2. We note that the pixels significant at 3σ are in the Enuc. 4 area. Three of the five pixels significant at 2σ are in the immediate vicinity of another star-forming region studied by Murphy et al. (2010) (i.e. Enuc. 6). The remaining two are located in the extended region of relatively bright 1 cm emission to the northeast of Enuc. 4 (see Figure 1).

4.2 AME per $M_{\text{PAH}}$

Using Equation 10 and the $q_{\text{PAH}}$ and $M_d$ values in each pixel as determined by Aniano et al. (2012), we predict the expected AME in each pixel from spinning dust emission. In Figure 1 we plot the value of $M_{\text{PAH}} = q_{\text{PAH}}M_d$ in each pixel against the 1 cm fit AME flux density $F_{\nu,1\text{ cm}}$ for the 8 AME detections. The regions are best fit by an emissivity of $(1.1 \pm 0.2) \times 10^{-7}$ Jy/$M_{\text{PAH}}$, in sharp tension with the $2 \times 10^{-8}$ Jy/$M_{\text{PAH}}$ typical of Galactic AME. Likewise, this value is too high to be consistent with the AME non-detections in the remainder of the galaxy as illustrated in Figure 1. Therefore, if the AME is rotational emission from small spinning grains, the emissivity must vary significantly even at a fixed number of small grains.

4.3 AME Detections vs. Non-Detections

If some regions of the galaxy produce significantly more AME per PAH mass than others, what sets these regions apart? We contrast the AME detections against the ensemble of pixels in both dust properties ($L_d$, $M_{\text{PAH}}$, $q_{\text{PAH}}$, ...).
Table 2. AME Detections

| Pixel | R.A.     | Dec.    | $F_{v,1\text{ cm}}$ | $F_{v,1\text{ cm}}^{\text{AME}}$ | $F_{v,100\mu\text{m}}$ | $F_{v,8\mu\text{m}}$ | $M_d$ | $q_{\text{PAH}}$ | $L_d$ | $U$ | $f_{\text{PDR}}$ | $\alpha$ | $\gamma$ | $\alpha_{\text{sync}}$ |
|-------|----------|---------|---------------------|-----------------------------------|------------------------|-----------------------|-------|-----------------|-------|-----|-----------------|---------|---------|---------------------|
| 1     | 308.5885 | 60.1654 | 635 ± 170           | 0.62                              | 1300                   | 0.67                  | 1.12  | 0.03            | 6.29  | 3.35| 0.13            | 1.62    | 0.00    | 0.67                |
| 2     | 308.5768 | 60.1653 | 443 ± 150           | 0.61                              | 1800                   | 0.62                  | 0.90  | 0.03            | 6.14  | 3.94| 0.12            | 1.81    | 0.06    | 0.79                |
| 3     | 308.5885 | 60.1712 | 714 ± 200           | 0.55                              | 1600                   | 0.48                  | 1.31  | 0.03            | 9.30  | 4.22| 0.17            | 1.78    | 0.01    | 0.56                |
| 4     | 308.7644 | 60.1771 | 833 ± 350           | 0.56                              | 2200                   | 0.88                  | 2.19  | 0.04            | 13.31 | 3.64| 0.12            | 1.52    | 0.00    | 1.12                |
| 5     | 308.7527 | 60.1771 | 730 ± 300           | 0.57                              | 2200                   | 0.94                  | 2.12  | 0.04            | 11.92 | 3.45| 0.11            | 1.51    | 0.00    | 1.17                |
| 6     | 308.7644 | 60.1829 | 813 ± 300           | 0.49                              | 3500                   | 0.71                  | 2.59  | 0.04            | 21.49 | 4.90| 0.14            | 1.58    | 0.00    | 0.93                |
| 7     | 308.6119 | 60.1829 | 374 ± 170           | 0.46                              | 1900                   | 0.87                  | 1.21  | 0.03            | 5.70  | 2.84| 0.10            | 1.47    | 0.00    | 1.00                |
| 8     | 308.6236 | 60.1887 | 364 ± 160           | 0.63                              | 1100                   | 1.00                  | 1.03  | 0.04            | 3.22  | 1.88| 0.08            | 1.64    | 0.01    | 1.15                |

Note— RA and Dec are reported at the centre of the 21″×21″ pixel. Thus, pixels in the same row or column of the gridded image will share an RA or Dec.

Figure 5. Fit residuals at 1 and 3 cm for radio models without an AME component. Panels (a) and (b) are for a constant synchrotron power law index while panels (c) and (d) are for an index that steepens infinitely at 3 cm, resulting in no 1 cm synchrotron emission. Both models strongly indicate the need for an AME component in some regions. The asymmetry in the residuals for the former model suggest that the radio emission is being over-estimated at 1 cm. This asymmetry is somewhat improved in the model with a steepening index, but some negative bias remains.

Figure 6. The PAH mass in each pixel in Table 2 is plotted against the fit AME flux density in that pixel. If the AME is arising from rotational emission from spinning grains, the two quantities should be roughly linearly correlated. We overplot the theoretical curve assuming linear correlation and using the canonical spinning dust emissivity (black dashed) as well as our best fit emissivity for the ensemble (red solid).

Performing a similar investigation within the Perseus molecular cloud, Tibbs et al. (2011) found that regions with AME tended to have stronger radiation fields than those without. Similarly, the strength of the radiation field was found to be correlated with the AME in the HII region RCW175 by Tibbs et al. (2012a). We also find a preference for larger $\bar{U}$ and $f_{\text{PDR}}$ values among our detections. Casassus et al. (2006) observed spinning dust emission in the PDR of LDN 1622, suggesting perhaps that spinning dust emission could be enhanced in these regions. We note that the physical scales in our study (≃ 1 kpc) are much larger than in these studies of Galactic clouds (≃ 1 – 10 pc). However, if the AME power is robust to environment as predicted by the spinning dust theory, we can make meaningful comparisons regardless of the size of the region. This is particularly true when comparing the AME power per $M_{\text{PAH}}$.

The ratio of the AME flux density at 30 GHz to the 100 µm flux density has been a common diagnostic in the literature. Davies et al. (2006) at intermediate latitudes and Alves et al. (2010) in the Galactic plane both derive a value of $3 \times 10^{-4}$; Todorović et al. (2010) find a mean ratio of $(1.08 \pm 0.02) \times 10^{-4}$ in Galactic HII regions; and Planck Collaboration et al. (2014) derive values for Galactic clouds of $(2.5 \pm 0.2) \times 10^{-4}$ and $(5.8 \pm 0.7) \times 10^{-4}$ us-
ing an unweighted and weighted mean, respectively. An unweighted mean of the values in our Table 2 yields a ratio of $(5.1 \pm 1.8) \times 10^{-4}$, consistent with previous results though the variance is large. A large scatter in this quantity is unsurprising given the dependence of the $100 \mu m$ flux on grain temperature (Tibbs et al. 2012b).

We also note that the majority of pixels with a ratio of $100 \mu m$ to 1 cm flux density of less than $\sim 1000$ are AME detections. While this in itself is unsurprising since regions with AME will be brighter at 1 cm than regions without, this suggests that this ratio could be a predictor of AME-positive regions using only these two bands.

There is also a distinct trend for the AME detections to be located in the spiral arms of the galaxy rather than the nuclear region. Additionally, it appears that there are large regions of AME emission that span multiple pixels, suggesting a “diffuse” origin of the AME rather than, e.g., compact HII regions.

### 4.4 Correlations with AME Intensity

We next examine correlations between the AME intensity and dust and environmental parameters. We find that, as expected, quantities that correlate with dust mass ($M_{PAH}, L_d, F_{\nu,100 \mu m}$) correlate with the fit AME intensity (Figures 6 and 8). Similarly, we find good correlations with the emission in all of the radio bands, in accord with observations of Galactic clouds by Planck (Planck Collaboration et al. 2014b). Finally, we also observe positive correlation between the AME intensity and emission in the radio bands, which is expected since both should correlate positively with the gas column. These correlations are summarised in Figure 8.

To probe variations in AME strength beyond what is expected simply from the amount of gas and dust in that region, we normalise the fit AME flux density by the dust mass in that pixel. This is the normalisation suggested by Tibbs et al. (2012b) who caution that the 100 $\mu m$ flux, often used instead, is temperature-sensitive. This normalisation is also directly comparable to the results of Planck Collaboration et al. (2014b) where the optical depth at 250 $\mu m$ $\tau_{250}$ was used as a normalisation.

In Figure 9 we plot $M_d, q_{PAH}, U$, and $f_{PDR}$ against the AME flux density normalised by the dust mass. Analysis of WMAP foregrounds by Lagache (2002) revealed that the AME per column decreases with increasing column, lending credence to the argument that AME is not arising from large grains. Planck Collaboration et al. (2014b) reports a sublinear correlation between the AME intensity and the gas column with a power law index of $0.33 \pm 0.04$. Likewise, studying AME in translucent clouds, Vidal et al. (2011) find that the AME intensity per gas column declines in proportion to the gas column. Among the AME detections in NGC 6946, we find a best fit power law index of $0.59 \pm 0.37$, in accord with the results from Vidal et al. (2011) and Planck Collaboration et al. (2014b), but limited by our small number of detections.

Although we find tentative agreement with the previous result that the AME is imperfectly correlated with the large grains, we find no better correlation with tracers of small grains. The relationship between $F_{\nu,37}^{AME}/M_d$ and $q_{PAH}$ is best fit by a power law index of $-0.56 \pm 0.62$ whereas the value assumed by Equation 10 is 1. A similar result is obtained using the 8 to 24 $\mu m$ ratio.

Ysard et al. (2010) find that over the whole sky the AME correlates better with the 12 $\mu m$ emission than the 100 $\mu m$ emission, although it was well-correlated with both. Similarly Casassus et al. (2006) found the AME in the dark cloud LDN 1622 to be better correlated with maps of the 12 and 25 $\mu m$ emission than the 100 $\mu m$ emission. These trends are not observed in a study of Galactic clouds by Planck Collaboration et al. (2014b), who find that the 12 $\mu m$ map is less correlated with AME than maps at 25, 60, or 100 $\mu m$. As pointed out by Tibbs et al. (2012b), correlations against 100 $\mu m$ are complicated by the dependence of the 100 $\mu m$ flux on grain temperature. Likewise, the 12 $\mu m$ emission depends not just upon the small grain population but also upon the strength of the radiation field. Taken together with our results, these data do not present a strong case for the association of AME with the smallest grains.

Previous work, both theoretical and observational, suggests an insensitivity of AME amplitude to the radiation field strength. In particular, Ysard & Verstraete (2010) find no correlation over three orders of magnitude in field strength. We likewise find no correlation, though our AME detections tend to be in regions of above average radiation field intensity. We similarly find no significant correlation of the AME intensity with $f_{PDR}$, though in both cases we are severely limited by the small number of detections.

### 5 DISCUSSION

The AME we observe in Enc. 4 and several other regions of NGC 6946 is inconsistent with Galactic AME per dust mass even though the AME per 100 $\mu m$ flux density in these regions falls within what has been observed in the Galaxy. Additionally, the emissivity per $M_{PAH}$ in these regions is incompatible with upper limits on the AME in other regions of NGC 6946. Therefore, the data suggest strong variation of the AME intensity at fixed $M_{PAH}$, a result unanticipated by theoretical models of spinning dust emission.

Although they did not estimate the population of small grains explicitly, Planck Collaboration et al. (2014b) found a scatter of roughly an order of magnitude in the AME in-
Figure 7. Histogram of various dust and environmental properties for the AME detections (red filled) and the ensemble of the pixels (black). For readability, we scale the number AME detections up by a factor of ten. No strong trends emerge from contrasting the two populations, although the regions with AME detections appear to favor larger $\bar{U}$ values.

Figure 9. We examine the correlations between the environment and the strength of the AME per dust mass in the eight regions listed in Table 2. As illustrated in panel (a), the AME flux density normalised by the dust mass is consistent with a negative correlation with dust mass, in accord with previous results that AME per column density decreases with column density. In panel (b), we find that a positive linear correlation with $q_{\mathrm{PAH}}$ is unfavored by the data. We note that replacing $q_{\mathrm{PAH}}$ with the ratio of 8 to 24 $\mu$m emission produces a nearly identical plot. In the remaining panels, we find no correlations between the normalised AME flux density and (c) $\bar{U}$ or (d) $f_{\mathrm{PDR}}$. However, the small sample size precludes drawing strong conclusions from the lack of any correlations.
tensity normalised by the optical depth at 250 μm in a sample of Galactic clouds. Correlation analysis with a suite of environmental parameters yielded no compelling drivers of increased emissivity, much in accord with our results here. Such variation is also evident in the Andromeda Galaxy, which has yielded only upper limits on an AME component despite observations with excellent frequency coverage from both WMAP and Planck and an ample dust reservoir in the galaxy (Ade et al. 2014). Recent determinations of the dust content of Andromeda by Draine et al. (2014) allow us to make a theoretical estimate of the expected spinning dust emission. Inserting the total derived dust mass of $5.4 \times 10^7 M_\odot$ and the global average value of $q_{\text{PAH}} = 0.036$ from Draine et al. (2014), and a distance of 744 kpc (Vilardell et al. 2010) into Equation 10 yields an AME flux density of 2.86 Jy. This value is comparable to the total observed 30 GHz emission of $2.55 \pm 0.44$ Jy and exceeds the $3\sigma$ upper limit placed on an AME contribution at that frequency of 2.2 Jy (Ade et al. 2014). However, the ratio of 100 μm to 30 GHz flux density is $7.1 \times 10^{-4}$, comparable to our detections and values obtained by Planck Collaboration et al. (2014b).

Peel et al. (2011) investigate the SEDs of three dusty star-forming galaxies (M82, NGC 253, and NGC 4945) for evidence of AME. Using a benchmark AME to 100 μm flux density of $3 \times 10^{-4}$, they find AME flux densities estimated from this ratio far in excess of the observed emission for all three galaxies. This result would be exacerbated using instead the average value of $5 \times 10^{-4}$ from our Table 2. Additionally, due to their excellent frequency coverage between 23 and 143 GHz, an AME component peaking at a frequency other than 30 GHz is unlikely to explain the missing flux.

In the context of spinning dust theory, the simplest explanation for variations in emission strength is variation in the abundance of small grains. However, this explanation is inconsistent with our data. We employ $q_{\text{PAH}}$ directly from fits to the thermal dust emission to minimise spurious correlation induced by, e.g., varying grain temperatures. The AME is not found preferentially in regions with large values of $q_{\text{PAH}}$, or even $M_{\text{PAH}}$. Additionally, a linear scaling of the AME intensity per $M_\odot$ with $q_{\text{PAH}}$ is disfavoured by our data at greater than 2σ. If the spinning dust paradigm is correct, and if certain regions of NGC 6946 have AME much stronger than what has been observed in, e.g., Galactic clouds, then an explanation must be furnished for why the small grains in these regions are producing electric dipole radiation in excess of the expected level. Likewise, if the spinning dust emissivity in Andromeda is indeed much weaker than in the Milky Way despite comparable populations of small grains, this must too be explained.

We examine a few possibilities that may reconcile the variation in emissivity with the theoretical expectations, but none appear able to adequately resolve the tension. First, we have considered only the emission at 30 GHz, but AME has been observed over a range of peak frequencies from about 20 to 50 GHz (e.g. Planck Collaboration et al. 2014b). It may be possible that regions like Enuc. 4 simply have AME peaking closer to 30 GHz than the typical diffuse ISM or Galactic clouds. However, if the AME were peaking at 20 GHz, the 30 GHz emission would be about two thirds the peak value assuming the spectrum of Equation 7. Likewise, if the AME peaked at 40 GHz, the 30 GHz amplitude would be lower than the peak amplitude by just over ten per cent. This effect is insufficient to account for the entirety of the variation in NGC 6946 and not permitted by the multi-frequency observations of Andromeda (Ade et al. 2014) or the star-forming galaxies of Peel et al. (2011).

Second, the derived value of $q_{\text{PAH}}$ does not correspond precisely to the total PAH fraction by mass. Rather, it is determined from the IR emission features and is therefore weighted toward regions with the high $U$ value. Thus, if there were a reservoir of cold dust that was significantly depleted in PAHs (due, for instance, to grain coagulation), then the derived $q_{\text{PAH}}$ would not reflect the true PAH mass of that region. However, the variations in $q_{\text{PAH}}$ with environment required to reconcile the data with the theoretical emissivity would appear to be far greater than the observed pixel-to-pixel variations of $q_{\text{PAH}}$ itself within the galaxy.

Third, $q_{\text{PAH}}$ traces only the abundance of ultrasmall carbonaceous grains. If the AME arises in parts or totally from ultrasmall grains of a different composition, such as ultrasmall silicates, then the abundance of AME-producing grains would not be accurately traced by $q_{\text{PAH}}$. However it is unclear why these grain populations would not vary cospatially nor does it seem likely that this could account for the entirety of the observed variations.

Finally, there exist mechanisms within the spinning dust theory that can alter the spinning dust emissivity. The typical electric dipole moment of a grain may vary from region to region due, for instance, to variations in grain asymmetry. However, we would expect these variations to be accompanied by environmental variations that explain the differences, such as a more intense radiation field, which we have not seen.

Taken in conjunction with the previous literature, our study suggests that the AME emissivity per $M_{\text{PAH}}$ varies by more than a factor of 10 between the Andromeda Galaxy, the diffuse ISM of the Milky Way, Galactic clouds, and certain extra-nuclear regions of NGC 6946. Without a clear means of discriminating between regions of particularly high or low AME, the spinning dust hypothesis is at best incomplete.

While we demonstrate the power of coupling AME observations with detailed modelling of the thermal dust component, we are limited by our frequency coverage and sensitivity. Follow-up observations that could better pin down the free-free component would be invaluable for more detailed SED modeling. In addition to mitigating a key uncertainty, such data would also allow exploration of the variations of the AME peak frequency with environmental parameters. Deeper 1 cm observations of NGC 6946 could better test whether the diffuse ISM of the galaxy has an AME emissivity consistent with Equation 10.

6 CONCLUSIONS

We have combined new 1 cm and 3 mm CARMA observations and 2 mm GISMO observations with existing IR and radio data to constrain the SED of the AME in NGC 6946. Our principal conclusions are as follows:

(i) We confirm the detection of AME by Murphy et al. (2010) in Enuc. 4 and find that the emission is well-fit by a spinning dust component having amplitude 0.9 mJy and peak frequency 42 GHz. The peak frequency corresponds
well with models of the CNM and WIM. However, the emissivity exceeds the theoretical value by about a factor of ten given its PAH surface density.

(ii) We find eight regions with AME significant at > 95% confidence. Multi-frequency follow-up observations of these regions are needed to confirm whether this excess is attributable to spinning dust emission. Such observations could further explore the spatial variations of the spinning dust emission within the galaxy, particularly dependence of the peak frequency on environment.

(iii) The strength of the AME in these regions is well-correlated with all tracers of dust and gas mass, and we derive a spinning dust emissivity of $1 \times 10^{-7}$ Jy/M$_{PAH}$ in these regions, a factor of five higher than the Galactic value.

(iv) Our results are consistent with previous studies that suggest the AME per unit column density declines with increasing column density. We find no indications that AME correlates with the presence of small grains or the intensity of the radiation field, though these conclusions are limited by a small sample size.

(v) The majority of locations in the galaxy are inconsistent with a spinning dust emissivity as strong as that observed in Enc. 4 given their PAH surface density. This suggests that, if indeed the AME is emission from spinning ultra-small grains, other environmental factors must influence the strength of the emission. However, we find no compelling environmental discriminator between regions with and without detected AME.

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