Physiologic Rate of Carrier-mediated Ca\(^{2+}\)
Entry Matches Active Extrusion in
Human Erythrocytes

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ABSTRACT The intracellular Ca\(^{2+}\) concentration of nearly all cells is kept at submicromolar levels. The magnitudes of transmembrane Ca\(^{2+}\) movement that maintain this steady state in the human red blood cell have long been debated. Although there is agreement that the physiologic extrusion of Ca\(^{2+}\) by the well-characterized Ca\(^{2+}\) ATPase amounts to 45 \(\mu\)mol/liter cells per h (1982. Nature (Lond.), 298:478–481), the reported passive entry rates in physiological saline (2–20 \(\mu\)mol/liter cells per h) are all substantially lower. This discrepancy could be due to incomplete inhibition of the pump in the previous measurements of Ca\(^{2+}\) entry. We therefore examined both rate and mechanism of entry after completely inactivating the pump. This required pretreatment with iodoacetamide (to lower the intracellular ATP concentration) and vanadate (to inhibit any residual Ca\(^{2+}\) pump activity). The rate of Ca\(^{2+}\) entry (53 \(\mu\)mol/liter cells per h) was now found to be comparable to the accepted extrusion rate. Entry closely obeyed Michaelis-Menten kinetics \((V_{\text{max}} = 321 \pm 17 \text{ nmol Ca/g dry wt per h}, K_m = 1.26 \pm 0.13 \text{ mM})\), was competitively inhibited by external Sr\(^{2+}\) \((K_i = 10.8 \pm 1.2 \text{ mM})\), and was accelerated by intracellular Ca\(^{2+}\). \(^{45}\)Ca\(^{2+}\) efflux from these pump-inactivated cells was also accelerated by either external Ca\(^{2+}\) or Sr\(^{2+}\). These accelerating effects of divalent cations on the opposite (trans) face of the membrane rule out a simple channel. Substrate-gated channels are also ruled out: cells equilibrated with \(^{45}\)Ca\(^{2+}\) lost the isotope when unlabeled Ca\(^{2+}\) or Sr\(^{2+}\) was added externally. Thus, passive Ca\(^{2+}\) movements occur predominantly by a reversible carrier-mediated mechanism for which Sr\(^{2+}\) is an alternate substrate. The carrier's intrinsic affinity constants for Ca\(^{2+}\) and Sr\(^{2+}\), 1.46 and 0.37 mM\(^{-1}\), respectively, indicate that Ca\(^{2+}\) is the preferred substrate.

INTRODUCTION

Fluctuations in the free intracellular Ca\(^{2+}\) concentration, [Ca\(^{2+}\)\], are thought to trigger many cellular processes by activating Ca\(^{2+}\)-dependent enzymes such as protein kinase C, actin-myosin ATPase, or the Ca\(^{2+}\)-dependent K\(^+\) channel. Steady-state [Ca\(^{2+}\)] is largely determined by the balance between the active extrusion and passive entry mechanisms present in the plasma membrane of most cells (Schatz-
mann, 1985). Despite the fundamental regulatory role of [Ca$^{2+}$], previously reported Ca$^{2+}$ entry and exit rates have not matched quantitatively under physiologic conditions.

In the red blood cell (RBC), active extrusion is mediated by an efficient Ca$^{2+}$ ATPase pump. This pump has been studied carefully (see Schatzmann, 1985, and Carafoli, 1987, for reviews); its high affinity for intracellular Ca$^{2+}$ maintains a steady-state [Ca$^{2+}$], of 20–30 nM (Lew et al., 1982), a value some 50,000-fold lower than the external free Ca$^{2+}$ concentration, [Ca$^{2+}$]$_o$.

In contrast, the downhill entry of Ca$^{2+}$ is poorly understood. $^{45}$Ca$^{2+}$ tracer fluxes reveal it only when the Ca$^{2+}$ pump is inhibited. While there are no complete and specific Ca$^{2+}$ pump inhibitors, several approaches—La$^{3+}$ blockade, ATP or Mg$^{2+}$ depletion (Ferreira and Lew, 1977; McNamara and Wiley, 1986), vanadate pretreatment (Varecka and Carafoli, 1982; Varecka et al., 1986), and Ca$^{2+}$ chelator loading (Lew et al., 1982; Tiffert et al., 1984)—have been used to study passive entry either by slowing the Ca$^{2+}$ pump or by lowering [Ca$^{2+}$]. With these various methods, diverse entry rates in physiological saline, 2–20 µmol/liter cells per h, have been reported, all substantially lower than the accepted rate of active extrusion, 45 µmol/liter cells per h (Lew et al., 1982). Both the diversity of entry rates and the apparent imbalance between entry and exit are consistent with incomplete levels of pump inhibition in these previous studies.

This paper examines the passive movement of Ca$^{2+}$ across the human RBC membrane under conditions that completely inactivate the Ca$^{2+}$ extrusion pump. Under these conditions, passive Ca$^{2+}$ movement is mediated almost exclusively by a reversible carrier which also transports Sr$^{2+}$. Our kinetic analysis indicates that this carrier mediates the entry of Ca$^{2+}$ without exchange for intracellular cations under physiologic conditions. This influx also matches the rate of active extrusion by the Ca$^{2+}$ pump, thus maintaining a steady state [Ca$^{2+}$].

**MATERIALS AND METHODS**

*Preparation and Storage of RBCs*

Human blood was drawn into CPD (citrate, phosphate, dextrose—an anticoagulant) and centrifuged at 1,500 g in a Sorvall GLC-2B centrifuge. The plasma was removed and the cells were stored at a hematocrit (Hct) of 70% in ADSOL (a preservative) at 4°C for up to 3 wk under sterile conditions. The rates of passive $^{45}$Ca$^{2+}$ movement did not change during this storage period.

*Frequently Used Media*

Several frequently used media have been assigned the following abbreviations:

Medium A: 130 mM KCl, 30 mM sucrose, 20 mM HEPES, pH adjusted to 7.4 with 5 N KOH.

Medium B: 80 mM KCl, 60 mM NaCl, 20 mM HEPES, pH adjusted to 7.4 with 5 N KOH.

Medium C: 130 mM KCl, 30 mM sucrose, 20 mM HEPES, 5 mM Na$_2$VO$_4$, 20 µM valinomycin, pH adjusted to 7.4 with 5 N KOH or 1 N HCl as required.
Reagents

Benz 2 (MAPTAM) was purchased from Calbiochem Corp. (La Jolla, CA). $^{45}$CaCl$_2$ and $^{90}$Sr(NO$_3$)$_2$ were obtained from Amersham Corp. (Arlington Heights, IL). All other reagents were of analytical grade and were obtained from Sigma Chemical Co. (St. Louis, MO).

$\text{Ca}^{2+}$ Pump Inactivation

RBCs were washed and the buffy coats were removed before ATP depletion with 6 mM iodoacetamide (a glycolytic inhibitor), 10 mM inosine (Lew, 1971), and 0.1 mM EGTA at 5% Hct and 37°C for 3 h (Ferreira and Lew, 1977). To produce as low an [ATP] as possible, two steps were taken to maximize the consumption of ATP during this incubation with iodoacetamide. First, ATP depletion was carried out in medium A, which contained 130 mM K$^+$, to facilitate ATP consumption by the Na$^+/K^+$ pump. Second, the ATPase inhibitor, vanadate, was added only after the incubation with iodoacetamide.

Vanadate (Bond and Hudgins, 1978; Niggli et al., 1981) was used to inhibit $\text{Ca}^{2+}$ pump activity remaining after ATP depletion. Preincubation with vanadate lasted at least 30 min to ensure its entry by the anion exchanger, a process with a $t_{1/2}$ of 4 min (Cantley et al., 1978).

$\text{Ca}^{2+}$ Chelator Loading

To measure zero trans influx rates, RBCs were loaded with the $\text{Ca}^{2+}$ chelator Benz 2 (Tsien, 1981) by adding 0.1 mM of the chelator’s acetoxymethyl tetraester (250 mM stock solution in DMSO) to the ATP depletion medium.

$\text{Ca}^{2+}$ Loading

Two methods were used to load cells with $\text{Ca}^{2+}$. To load $^{45}$Ca$^{2+}$ concentrations $\leq$0.4 mM for efflux studies, ATP-depleted cells were incubated with 1 or 2 mM [$^{45}$Ca$^{2+}$], at 5% Hct and 35°C with continuous stirring for up to 50 h under sterile conditions. When a higher [Ca$^{2+}$] was desired, 0.1 $\mu$M A23187, a Ca$^{2+}$ ionophore, was used with 4 mM [Ca$^{2+}$], (see legend of Fig. 3 A for details).

Measurement of RBC $^{45}$Ca$^{2+}$ Content

RBC $^{45}$Ca$^{2+}$ flux was terminated by three to four rapid washes in ice-cold medium A with 1 mM EGTA (which required ~2 min) and centrifugation through a 4:1 silicone/mineral oil mixture at 11,000 g for 10 s. The pellet was then digested in a 1:2 Protosol$^\text{®}$ (tissue solubilizer)/ethanol mixture, decolorized with 30% H$_2$O$_2$, and neutralized with 1 N HCl before $\beta$-counting in 8 ml of Universol$^\text{®}$ scintillation cocktail.

Establishment and Determination of a Donnan Membrane Potential

A constant, known $V_m$ (membrane potential) was required to rule out kinetic artifacts due to a changing $V_m$ and to calculate the carrier’s intrinsic affinity constants for $\text{Ca}^{2+}$ and Sr$^{2+}$. To establish Donnan equilibrium, ATP-depleted RBCs were incubated in medium C (which contained 20 $\mu$M valinomycin, a K$^+$ ionophore) for 7 h before $^{45}$Ca$^{2+}$ flux measurements. To estimate the Donnan $V_m$, these cells were packed in a 400-$\mu$L microfuge tube by centrifugation at 11,000 g for 15 min and collected after cutting the tube below the cell–saline interface (extracellular trapping 1.5% by volume using $^{45}$Ca$^{2+}$-EGTA). After weighing, the cells were lysed in 1,000 vol of distilled H$_2$O to determine their intracellular K$^+$ content with a model 251 atomic absorption spectrophotometer (Instrumentation Laboratory, Inc., Lexington, MA). K$^+$
standards were prepared in the same distilled H2O. The K⁺ content was converted to an intracellular K⁺ concentration using the percent cell H2O by weight, which was determined using equivalent samples weighed before and after drying to constant weight at 70°C. \( V_{m} \), calculated using the Nernst equation for K⁺, reached a steady-state value of \(-4 \text{ mV}\), in good agreement with the predicted Donnan \( V_{m} \) of \(-7 \text{ mV}\) for medium C (Freedman and Hoffman, 1979).

**Units of Flux Measurements**

Rates of transport are reported in nanomoles per gram dry weight per hour, rather than micromoles per liter cells per hour, because the former is readily converted to rates per RBC (grams dried cell solids = \(3.1 \times 10^{10}\) RBCs) without correcting for variations in cell volume (Weith et al., 1974). In each experiment, an equivalent sample of RBCs, taken immediately before the flux measurement, was dried as above and used to calibrate the measured rates. Hemolysis during the 1 h required to measure entry rates (Fig. 2) was < 2% (determined by weighing RBC samples collected after the flux measurements) and was ignored.

**RESULTS**

**Complete Inactivation of the Ca²⁺ Pump**

After pretreatment with 6 mM iodoacetamide, 0.5 mM vanadate was required to block residual Ca²⁺ pump activity. Higher vanadate concentrations had no further effect on the \(^{45}\)Ca²⁺ efflux rate. Thus, the Ca²⁺ pump was completely inactivated (legend, Fig. 1 A) and any remaining \(^{45}\)Ca²⁺ efflux was passive.

**Unidirectional Passive Influx**

The unidirectional influx rate could now be measured by adding extracellular \(^{45}\)Ca²⁺ after the cells were loaded with the Ca²⁺ chelator Benz 2. In cells not so loaded (Fig. 1 B, filled circles) the rate of accumulation decreased gradually, mainly because of increasing passive \(^{45}\)Ca²⁺ efflux. In Benz 2–loaded cells, the intracellular chelator allowed a constant rate of \(^{45}\)Ca²⁺ accumulation for ~ 2 h (Fig. 1 B, filled triangles). The identical initial influx rates with or without Benz 2 indicate that the chelator does not affect RBC Ca²⁺ permeability.

The omission of vanadate produced substantially lower influx (Fig. 1 B, open symbols). Thus, even after ATP depletion and Benz 2–loading, vanadate was required to inhibit residual Ca²⁺ pumping. Indeed, these data demonstrate why previously reported entry rates (measured after either ATP depletion or exposure to vanadate, but not both) were two- to threefold lower than required to match physiologic Ca²⁺ pumping.

At \([\text{Ca}^{2+}]_o < 5 \text{ mM}\), influx obeys Michaelis-Menten kinetics, suggesting a saturable process and the translocation of one Ca²⁺ ion per reaction cycle. At higher \([\text{Ca}^{2+}]_o\) (5–30 mM), a nonsaturating component becomes apparent (Fig. 2). The unidirectional \(^{45}\)Ca²⁺ influx rates \((v)\), observed at different \(\text{Ca}_o\), were fitted with:

\[
v = \frac{V_{\text{max}} \times \text{Ca}_o}{K_m + \text{Ca}_o} + L \times \text{Ca}_o
\]

using the nonlinear, weighted, least-squares method (De Weer and Lowe, 1973).
Figure 1. Unidirectional passive Ca\(^{2+}\) transport. (A) Effect of vanadate on Ca\(^{2+}\) efflux from ATP-depleted RBCs. ATP-depleted, \(^{45}\)Ca\(^{2+}\)-loaded RBCs were washed and resuspended at 37°C and 0.2% Hct in medium B with 1 mM EGTA and 0 mM (triangles), 0.5 mM (circles), or 2.5 mM (diamonds) Na\(_3\)VO\(_4\) at pH 7.4. Solid lines in this figure and in Figs. 1 B, 3, A and B, 4 C, and 7 represent least-squares fits of single exponentials. Notice that increasing the [VO\(_4\)\(^{3-}\)] fivefold (from 0.5 to 2.5 mM) had no further effect on the rate of \(^{45}\)Ca\(^{2+}\) efflux. (B) Effect of Benz 2 on passive Ca\(^{2+}\) accumulation. ATP-depleted RBCs with (triangles) or without (circles) Benz 2 loading were incubated in medium A with 2.5 mM Na\(_3\)VO\(_4\) at pH 7.4 for 2 h (filled symbols). To measure \(^{45}\)Ca\(^{2+}\) accumulation (0.5 mM \(^{45}\)CaCl\(_2\)), these RBCs were incubated at 20% Hct and 37°C in medium A with (filled symbols) or without (open symbols) 2.5 mM Na\(_3\)VO\(_4\) (pH 7.4). [VO\(_4\)\(^{3-}\)] greater than 2.5 mM did not further increase influx, indicating that the Ca\(^{2+}\) pump was completely inactivated (not shown).

Estimates of the parameters and their standard errors were \(V_{\text{max}} = 291 \pm 18\) nmol Ca/g dry wt per h, \(K_m = 1.10 \pm 0.12\) mM, and \(L = 13.94 \pm 1.00\) nmol Ca/(g dry wt per h per mM). To achieve a constant residual variance over the range of \([\text{Ca}^{2+}]_o\), the data were weighted by \(1/s^2\) in the least-squares algorithm. This weighting did not

Figure 2. Unidirectional passive \(^{45}\)Ca\(^{2+}\) influx rates at various \([\text{Ca}^{2+}]_o\). ATP-depleted, Benz 2–loaded RBCs were preincubated in medium C for 7 h at 37°C before measuring influx rates in the same medium with \(^{45}\)CaCl\(_2\). Solid line is the best fit to Eq. 1. Medium C contained negligible contaminant Ca\(^{2+}\) (<5 \(\mu\)M by atomic absorption) and its nominal \([\text{Ca}^{2+}]_o\) was not altered by adding RBCs, ruling out artifactual causes for the nonlinear flux concentration profiles. These rates were unchanged when valinomycin was omitted or when the vanadate concentration was raised from 5 to 10 mM. Thus, these agents do not alter RBC Ca\(^{2+}\) permeability.
significantly alter parameter estimates, but was required to satisfy the constant variance assumption used to estimate standard errors (Draper and Smith, 1981).

For physiologic \([\text{Ca}^{2+}]_o\) (1.3 mM) influx is 176 nmol/g dry wt per h or 53 \(\mu\)mol/liter cells per h, in good agreement with the known physiologic \(\text{Ca}^{2+}\) pump rate of 45 \(\mu\)mol/liter cells per h (Lew et al., 1982). Replacement of KCl by NaCl produced no changes in \(^{45}\text{Ca}^{2+}\) influx or efflux rates and thus ruled out a \(\text{Na}^+ / \text{Ca}^{2+}\) exchanger (data not shown).

![Figure 3](image-url)

**Figure 3.** Trans acceleration. (A) Effect of \(\text{Trans} \text{Ca}^{2+}\) on passive \(^{45}\text{Ca}^{2+}\) influx. After ATP depletion without \(\text{Benz} 2\) loading, RBCs were incubated at 5% Hct and 37°C for 18 h in medium C (triangles), in medium C with 0.1 \(\mu\)M A23187 and 0.1 mM EGTA (diamonds), or in medium C with 0.1 \(\mu\)M A23187 and 4 mM unlabeled \(\text{CaCl}_2\) (circles). RBCs exposed to A23187 were then washed five times at a Hct of 5% in medium A with 50 \(\mu\)M BSA at pH 7.4. After three additional washes in medium C, \(^{45}\text{Ca}^{2+}\) accumulation was measured in medium C with 1 mM \(^{45}\text{Ca}^{2+}\). The ionophore concentration used was sufficient to load 4 mM unlabeled \(\text{Ca}^{2+}\) into RBCs, yet low enough that five BSA washes (Simonsen, 1980) restored the original \(\text{Ca}^{2+}\) permeability of the cells (compare diamonds and triangles). (B) Effect of \(\text{Trans} \text{Ca}^{2+}\) on passive \(\text{Ca}^{2+}\) efflux. The time course of \(^{45}\text{Ca}^{2+}\) efflux from ATP-depleted, \(^{45}\text{Ca}^{2+}\)-loaded RBCs was followed in medium C with either 0.1 mM EGTA (triangles) or 10 mM \(\text{CaCl}_2\) (circles).

**Effects of Trans Unlabeled \(\text{Ca}^{2+}\)**

To distinguish between the two simplest kinetic models for passive transport that obey Michaelis-Menten kinetics, the channel and carrier models (Stein, 1986), influx and efflux of \(^{45}\text{Ca}^{2+}\) were examined with and without unlabeled \(\text{Ca}^{2+}\) on the trans side. Influx was studied in cells loaded with millimolar \(\text{Ca}^{2+}\) by incubation with 4 mM \([\text{Ca}^{2+}]_o\), and the \(\text{Ca}^{2+}\) ionophore A23187. After washing the cells with BSA to remove all detectable ionophore activity, \(^{45}\text{Ca}^{2+}\) influx into these cells was threefold that into cells not loaded with \(\text{Ca}^{2+}\) (Fig. 3 A, legend). Similarly, efflux from cells loaded with...
was accelerated by raising external \( \text{Ca}^{2+} \) from low nanomolar levels (with 0.1 mM EGTA) to 10 mM (Fig. 3 B). These \textit{trans} accelerations are incompatible with a simple channel and favor a carrier model (Lieb, 1982).

**Effects of Cis and Trans \( \text{Sr}^{2+} \) on the Proposed \( \text{Ca}^{2+} \) Carrier**

\( \text{Sr}^{2+} \) added to the extracellular medium competitively inhibited \( \text{Ca}^{2+} \) influx (Fig. 4, A [inset] and B). For \( \text{Sr}^{2+} \) concentrations up to 22.5 mM, the rate of \( ^{45}\text{Ca}^{2+} \) entry is given by:

\[
V = \frac{V_{\text{max}} \times C_{\text{ao}}}{K_v(1 + K_i/C_{\text{ao}})} + L \times C_{\text{ao}}
\]

(The second term represents the nonsaturating component described above.) The data fitted with this equation by the nonlinear, weighted, least-squares method yielded values for \( V_{\text{max}} \) of 321 ± 17 nmol Ca/g dry wt per h, for \( K_v \) of 1.26 ± 0.13 mM \( \text{Ca}^{2+} \), for \( K_i \) of 10.8 ± 1.2 mM \( \text{Sr}^{2+} \), and for \( L \) of 11.4 ± 0.9 nmol Ca/g dry wt/h per mM (Fig. 4 A). These estimates of \( V_{\text{max}} \) and \( K_v \) agree well with those obtained without \( \text{Sr}^{2+} \) (Fig. 2), verifying that simple competitive inhibition adequately describes the effect of external \( \text{Sr}^{2+} \) and that the \( \text{Ca}^{2+} \) carrier also binds \( \text{Sr}^{2+} \).

If the carrier could bind but not translocate \( \text{Sr}^{2+} \), \textit{trans} \( \text{Sr}^{2+} \) would inhibit \( ^{45}\text{Ca}^{2+} \) flux; if, instead, \( \text{Sr}^{2+} \) were also translocated, acceleration by \textit{trans} \( \text{Sr}^{2+} \) might be seen. Our data indicate that \( \text{Sr}^{2+} \) is transported: \textit{trans} \( \text{Sr}^{2+} \) accelerated \( ^{45}\text{Ca}^{2+} \) efflux markedly (Fig. 4 C). We could not test for the acceleration of \( ^{45}\text{Ca}^{2+} \) influx by \textit{trans} \( \text{Sr}^{2+} \) because we were unable to prepare cells loaded with millimolar \( \text{Sr}^{2+} \) (determined using \( ^{90}\text{Sr}^{2+} \); not shown).

**Testing a Substrate-gated Channel Model**

The observed acceleration of passive \( ^{45}\text{Ca}^{2+} \) transport by \textit{trans} \( \text{Ca}^{2+} \) and \textit{trans} \( \text{Sr}^{2+} \) (Figs. 3, A and B, and 4 C) suggests a simple carrier which presents its binding site to one side of the membrane at a time (Lieb, 1982). Although a simple channel can exhibit only \textit{trans} inhibition (Läuger, 1980) and is thus incompatible with our observations, a channel gated by \( \text{Ca}^{2+} \) and \( \text{Sr}^{2+} \) could in principle exhibit \textit{trans} acceleration. Such a channel would require positive gating by \textit{trans} \( \text{Ca}^{2+} \) and \( \text{Sr}^{2+} \) in both directions as well as competitive inhibition by \textit{cis} \( \text{Sr}^{2+} \). These are complicated constraints indeed. To distinguish unambiguously between the substrate-gated channel and simple carrier models, we added external unlabeled \( \text{Ca}^{2+} \) or \( \text{Sr}^{2+} \) to cells in which \( ^{45}\text{Ca}^{2+} \) was at electrochemical equilibrium. Added substrate might increase the permeability of a gated channel, but cannot provide the energy to drive label away from equilibrium because label and added substrates move independently (Fig. 5, \textit{dashed line}). For a simple carrier, however, labeled and unlabeled substrates do not move independently. The imposed inward gradient of unlabeled substrate could drive label out by countertransport. In our experiment the cells in fact lost \( ^{45}\text{Ca}^{2+} \), confirming the simple carrier model and ruling out a substrate-gated channel (Fig. 5).
FIGURE 4. Evidence suggesting that Sr$^{2+}$ is an alternate substrate. (A) Effect of cis Sr$^{2+}$ on unidirectional passive 45Ca$^{2+}$ influx. (Inset) The time course of 45Ca$^{2+}$ accumulation in medium C is shown for 0.7 mM 45Ca$^{2+}$ with either 0 mM (triangles) or 15 mM SrCl$_2$ (circles). Solid lines were determined by linear regression. In the main figure, 45Ca$^{2+}$ influx rates were measured as in Fig. 2 for [Ca$^{2+}$]$_o$ ranging from 0.3 to 30 mM with 0, 7.5, 15, and 22.5 mM SrCl$_2$. Each point represents the influx rate estimated using 5–15 45Ca$^{2+}$ accumulation time points (data for [Ca$^{2+}$]$_o$ < 10 mM and [Sr$^{2+}$]$_o$ = 0 and 22.5 mM shown). Solid lines represent the nonlinear, weighted, least-squares fit to Eq. 2. Examination of weighted residuals revealed that the fit was equally good for all [Ca$^{2+}$]$_o$ and [Sr$^{2+}$]$_o$. (B) Effect of cis Sr$^{2+}$ on passive 45Ca$^{2+}$ influx: Lineweaver-Burk plot. The data described in the main figure of A are replotted on a Lineweaver-Burk plot after correction for nonsaturating uptake by subtracting $L \times Ca_o (L = 11.4$ nmol Ca/[g dry wt/h per mM]). The solid lines represent the expected values calculated using the best estimates of $K_{m}$, $V_{max}$, and $K_s$ by Sr$^{2+}$ determined in Fig. 4 A (values listed in the text). A slightly better fit was obtained if Sr$^{2+}$ inhibition of the nonsaturating component (~20% at the highest [Sr$^{2+}$]$_o$) was permitted (not shown here). (C) Effect of trans Sr$^{2+}$ on passive 45Ca$^{2+}$ efflux. 45Ca$^{2+}$ efflux was followed in medium C with either 0.1 mM EGTA (triangles; same data as in Fig. 3 B) or 10 mM SrCl$_2$ (circles).
Figure 5. Effect of external unlabeled Ca$^{2+}$ or Sr$^{2+}$ on $^{45}$Ca$^{2+}$ equilibrium distribution. ATP-depleted RBCs were loaded with $^{45}$Ca$^{2+}$ by incubation in medium C with 1.0 mM $^{45}$CaCl$_2$ at 35°C for 39 h with continuous stirring, then washed and resuspended in medium C with 0.18 mM $^{45}$CaCl$_2$ (at the same specific activity) at 37°C for 12 h to demonstrate that the $^{45}$Ca$^{2+}$ content of the cells had come to equilibrium (triangles). At $t = 0$, 0.8 mM unlabeled CaCl$_2$ (open circles) or 0.8 mM SrCl$_2$ (filled circles) was added without significant dilution. The observed subsequent decrease in $^{45}$Ca$^{2+}$ content rules out substrate-gated channels, for which no change is expected (dashed line). Although this decrease should be transient, recovery could not be demonstrated because hemolysis did not permit quantitative measurements beyond 5 h. Before the addition of CaCl$_2$ or SrCl$_2$, intracellular free $^{45}$Ca$^{2+}$ was calculated to be 0.24 mM based on a membrane potential of -4 mV.

Our kinetic findings are most conservatively explained by a simple carrier with two charged substrates, Ca$^{2+}$ and Sr$^{2+}$:

\[
\begin{align*}
EP_0 & \underset{h_2}{\overset{h_1}{\rightleftharpoons}} EP_1 \\
E & \underset{k_2}{\overset{k_1}{\rightleftharpoons}} E \\
ES & \underset{g_2}{\overset{g_1}{\rightleftharpoons}} ES \\
ES_0 & \underset{f_2}{\overset{f_1}{\rightleftharpoons}} ES_i \\
ES_0 & \overset{b_2}{\rightleftharpoons} ES_i \\
E & \overset{d_2}{\rightleftharpoons} E \\
EP & \overset{d_1}{\rightleftharpoons} EP_i \\
EP_0 & \overset{\varepsilon_1}{\rightleftharpoons} EP_i \\
EP & \overset{\varepsilon_0}{\rightleftharpoons} EP_i
\end{align*}
\]

Scheme 1

In this scheme, E (enzyme) represents the unbound carrier, while ES and EP represent the carrier bound to substrates S or P, which stand for Ca$^{2+}$ and Sr$^{2+}$, respectively. Subscripts o and i refer to the outward- and inward-facing carrier intermediates. Lowercase letters represent first-order rate constants for each of the 14 allowed reactions (arrows). Pseudo-first-order rate constants (rate constants multiplied by appropriate free substrate concentrations) are also indicated. Slippage, the interconversion of E$_o$ and E$_i$ without Ca$^{2+}$ or Sr$^{2+}$ transport, is necessary to explain the $^{45}$Ca$^{2+}$ fluxes observed without trans substrate (e.g., efflux into EGTA-containing solutions [Fig. 1 A] or influx into Benz 2-loaded cells [Fig. 1 B]).

The unidirectional influx and efflux rates, $v_o$ and $v_i$, for the carrier in Scheme 1, derived using the method described in Stein (1986), are given by Eqs. A1 and A2 in the Appendix. These equations are of the most general form. Their derivation did
not require assumptions of rate-limiting steps or special electric field distributions in
the membrane. The rate equations have been used to further test the carrier model.
In particular, the carrier’s intrinsic affinities for Ca\textsuperscript{2+} and Sr\textsuperscript{2+}—K\textsubscript{ca} and K\textsubscript{sr}—were
determined by two methods, the concentration dependence of \textit{trans} acceleration and
the null point determination.

\textit{Concentration Dependence of Trans Acceleration: Estimation of K\textsubscript{ca}/K\textsubscript{sr}}

\textit{Trans} acceleration of \textsuperscript{45}Ca\textsuperscript{2+} efflux has been shown qualitatively in Figs. 3 B and 4 C.
To analyze \textit{trans} acceleration quantitatively, the initial rates of \textsuperscript{45}Ca\textsuperscript{2+} efflux were
measured with a range of unlabeled [Ca\textsuperscript{2+}]\textsubscript{o} and [Sr\textsuperscript{2+}]\textsubscript{o} (Fig. 6, A and B, respectively).
The unidirectional rate of \textsuperscript{45}Ca\textsuperscript{2+} efflux with \textit{trans} Ca\textsuperscript{2+} is given by:

\[ u_{st} = \frac{V^m + K_{ca} \times C_{ao}}{1 + K_{ca} \times C_{ao}} \] 

where \( V^m \) is the rate of efflux for zero Ca\textsubscript{o} and \( K_{ca}/K_{sr} \) is the rate for infinite Ca\textsubscript{o}. This
equation was derived by assuming zero [Sr$^{2+}$], zero [Sr$^{2+}$], and constant [Ca$^{2+}$] in Eq. A2. Thus, it describes for a simple Ca$^{2+}$ carrier how $v_{ef}$ should vary with [Ca$^{2+}$]. The analogous equation for 45Ca$^{2+}$ efflux with trans [Sr$^{2+}$], $S_{ro}$, was derived by setting [Ca$^{2+}$] and [Sr$^{2+}$], equal to zero in Eq. A2 and is:

$$v_{ef} = \frac{V_0 + \exp(-2u) \times K_{1Sr} \times S_{ro}}{1 + K_{2Sr} \times S_{ro}}$$

Here, $\exp(-2u)$ describes the effect of a nonzero membrane potential (see Eq. A3) on the acceleration of 45Ca$^{2+}$ efflux by Sr$^{2+}$. In these equations, the five constants ($V_0$, the two $K$'s, and the two $K$'s) result from regroupings of terms in Eq. A2 to define the concentration dependence of trans acceleration. These constants are functions of the 14 first-order rate constants in Scheme 1, the membrane potential, and [Ca$^{2+}$] (which changed <20% during the measurement of initial rates). The initial efflux rates in

![Image of Figure 7](image-url)

**Figure 7.** Effects of external 4°Ca$^{2+}$ and 45Ca$^{2+}$ on 45Ca$^{2+}$ equilibrium. RBCs were ATP-depleted and loaded with 45Ca$^{2+}$ as described in Fig. 5. After demonstrating that the isotope was at equilibrium (triangles), [45Ca$^{2+}$] and [4°Ca$^{2+}$], were changed to the values indicated. The inward 4°Ca$^{2+}$ movement due to raising [45Ca$^{2+}$] to 0.35 mM was balanced by the outward 45Ca$^{2+}$ movement due to raising [4°Ca$^{2+}$], to 0.48 mM. These values were used, along with $u$ (Fig. 6 B) and an initial [45Ca$^{2+}$] of 0.24 mM (electrochemical equilibrium with [4°Ca$^{2+}$], of 0.18 mM), to calculate $K_{ca}$ (Eq. 7).

Fig. 6, A and B, were fitted to Eqs. 3 and 4, respectively, by the unweighted least-squares method to obtain estimates for the five constants in these two equations. Using Eqs. 3, 4, and A2, the ratio of intrinsic affinities for Ca$^{2+}$ and Sr$^{2+}$ is given by:

$$K_{Ca}/K_{Sr} = \frac{K_{1ca}}{K_{1Sr}}$$

Thus, using the estimates for $K_{1ca}$ (Fig. 6 A) and $K_{1Sr}$ (Fig. 6 B), $K_{Ca}/K_{Sr}$ was 3.95. This finding is qualitatively consistent with Fig. 5, in which external unlabeled Ca$^{2+}$ had a greater effect on 4°Ca$^{2+}$ equilibrium than did external Sr$^{2+}$.

**Null Point Determination of Intrinsic Affinities**

The experiment shown in Fig. 7 was used to determine $K_{Ca}$ and $K_{Sr}$ explicitly; its design is based on changes in [45Ca$^{2+}$] seen after adding external labeled and unlabeled substrate to cells at 4°Ca$^{2+}$ equilibrium. For this experiment, it is necessary...
to consider the concentrations of $^{45}\text{Ca}^{2+}$ and unlabeled Ca$^{2+}$ separately. Adding external unlabeled Ca$^{2+}$ without changing $[^{45}\text{Ca}^{2+}]_o$ (Fig. 7, open circles) decreased $[^{45}\text{Ca}^{2+}]_i$ as seen previously (Fig. 5). In contrast, raising only $[^{45}\text{Ca}^{2+}]_o$ (filled circles) produced an increase in $[^{45}\text{Ca}^{2+}]_i$ because of carrier-mediated transport down an inward gradient. When both unlabeled Ca$^{2+}$ and $^{45}\text{Ca}^{2+}$ are added externally, the net effect on $[^{45}\text{Ca}^{2+}]_i$ depends on the relative magnitudes of the inward and outward driving forces produced by increasing $[^{45}\text{Ca}^{2+}]_o$ and unlabeled [Ca$^{2+}$]$_o$, respectively. When these two forces are equal, there is no initial change in $[^{45}\text{Ca}^{2+}]_i$ and the unidirectional fluxes in the two directions (Eqs. A1 and A2) are equal and opposite:

$$v_i - v_{ef} = 0$$  \hspace{1cm} (6)

Combining Eqs. 6, A1, and A2, the intrinsic affinity for Ca$^{2+}$ is:

$$K_{Ca} = \frac{4^{5}\text{Ca}_o - \exp(2u) \times 4^{5}\text{Ca}_i}{4^{5}\text{Ca}_m 4^{5}\text{Ca}_o - 4^{5}\text{Ca}_m \times 4^{5}\text{Ca}_i}$$  \hspace{1cm} (7)

where $4^{5}\text{Ca}_o$, $4^{5}\text{Ca}_m$, $4^{5}\text{Ca}_i$, and $4^{6}\text{Ca}_o$ represent the free concentrations of labeled and unlabeled Ca$^{2+}$ on the two sides of the membrane, which result in no net movement of $^{45}\text{Ca}^{2+}$ across the membrane. This condition was satisfied by a $4^{5}\text{Ca}_o$ of 0.35 mM and a $4^{6}\text{Ca}_o$ of 0.48 mM (Fig. 7, squares). By substituting these values into Eq. 7, $K_{Ca}$ is estimated to be 1.46 mM$^{-1}$. In a similar experiment where $[^{45}\text{Ca}^{2+}]_o$ and $[^{40}\text{Sr}^{2+}]_o$ were added (not shown), the estimate of $K_{Sr}$ ranged from 0.2 to 0.5 mM$^{-1}$, consistent with the ratio $K_{Ca}/K_{Sr} = 3.95$, estimated by the quantification of trans acceleration above. Using that ratio, the best estimate for $K_{Sr}$ is $K_{Ca}/3.95 = 0.37$ mM$^{-1}$.

**DISCUSSION**

We examined the rate and mechanism of passive Ca$^{2+}$ movement across the human RBC membrane. Although others have examined passive Ca$^{2+}$ entry (Ferreira and Lew, 1977; Varecka and Carafoli, 1982; Tiffert et al., 1984; McNamara and Wiley, 1986; Varecka et al., 1986), their accumulation measurements were offset by residual Ca$^{2+}$ pump activity. These previous workers did not use ATP depletion and vanadate pretreatment simultaneously and thus did not completely inactivate the pump (Fig. 1). Because of an incompletely blocked Ca$^{2+}$ pump, their estimates for the physiologic rate of Ca$^{2+}$ entry, 2–20 μmol/liter cells per h, failed to match the accepted rate of active extrusion by the Ca$^{2+}$ pump, 45 μmol/liter cells per h (Lew et al., 1982). Finally, the apparent saturability they observed is ambiguous: a nonsaturating leak offset by residual Ca$^{2+}$ pump activity could also produce net saturable entry.

The findings of Lew et al. (1982) deserve special consideration. They found an entry rate of 48 μmol/liter cells per h into chelator-loaded RBCs in autologous plasma. This value matches their measured rate of extrusion, 45 μmol/liter cells per h. Nevertheless, in physiological saline they found a rate of only 17 μmol/liter cells per h with ATP-depleted, chelator-loaded cells (Fig. 3 of Lew et al., 1982). Our Fig. 1 B demonstrates that 2.5 mM vanadate must also be added to completely inhibit the Ca$^{2+}$ pump in saline. Had they included vanadate in their experiment, the influx would have been approximately threefold greater and would have matched the
pump-mediated extrusion rate. These results suggest that there might be an endogenous Ca\(^{2+}\) pump inhibitor in plasma; this possibility warrants further study.

In saline, Ca\(^{2+}\) pump activity remains even when [ATP] is reduced to <2 \(\mu\)M by ATP depletion (Ferreira and Lew, 1977). We, therefore, added vanadate to completely inactivate the Ca\(^{2+}\) pump (Fig. 1, A and B). Under these conditions, passive Ca\(^{2+}\) entry was mediated almost exclusively by a simple carrier. Its rate (53 \(\mu\)mol/liter cells per h) then matches the rate of active extrusion under physiologic conditions.

Competitive inhibition by \(\text{cis SR}^{2+}\) (Fig. 4, A and B) and acceleration by \(\text{trans SR}^{2+}\) (Fig. 4 C) indicate that the carrier can also transport Sr\(^{2+}\). Two other group II divalent cations, Mg\(^{2+}\) and Ba\(^{2+}\), were less effective in their ability to competitively inhibit and \(\text{trans}\) accelerate \(^{45}\text{Ca}^{2+}\) movement (data not shown). Mg\(^{2+}\) was a particularly poor substrate for the carrier, consistent with the biological need to discriminate between Ca\(^{2+}\) and Mg\(^{2+}\) (Williams, 1980). Furthermore, if Mg\(^{2+}\) were a good substrate, the large inward Ca\(^{2+}\) gradient established by the Ca\(^{2+}\) pump would drive Mg\(^{2+}\) extrusion by the carrier. Because of the extremely low permeability of the RBC membrane to Mg\(^{2+}\) (Ginsburg et al., 1962), this would reduce \([\text{Mg}^{2+}]_i\) from its near-equilibrium value of 0.4 mM (Flatman and Lew, 1980) to levels much lower than needed for several critical enzymes (Wacker, 1969; Flatman and Lew, 1981).

The observed acceleration of passive \(^{45}\text{Ca}^{2+}\) transport by \(\text{trans Ca}^{2+}\) and \(\text{trans Sr}^{2+}\) (Figs. 3, A and B, and 4 C) suggests a simple carrier (Scheme 1). This model was tested quantitatively by determining the intrinsic affinities, \(K_c^a\) and \(K_{sr}\). These constants weight all substrate concentrations appearing in the rate equations, Eqs. A1 and A2, and are thus the best indicators of the carrier's substrate preference. Also, because of their ubiquitous appearance in Eqs. A1 and A2, the intrinsic affinities are determinable by more than one experimental approach. We were technically able to apply two approaches, the \(\text{trans}\) substrate concentration dependence and the null point methods. Similar values for \(K_c^a/K_{sr}\) were obtained by both methods, strongly supporting the simple carrier model (Stein, 1986). The relative magnitudes of \(K_c^a\) and \(K_{sr}\) indicate that Ca\(^{2+}\) is the preferred substrate by fourfold (Figs. 5-7).

Other carriers such as the \(\text{Cl}^-/\text{HCO}_3^-\) (Kaplan et al., 1983; Fröhlich, 1984) and \(\text{Na}^+/\text{H}^+\) (Aronson, 1985) exchangers function primarily as one-for-one exchangers with only rare slippage events. Indeed, those carriers may be able to release transported substrate only after binding the next substrate molecule, inconsistent with the model in Scheme 1. This would minimize slippage by disallowing the unloaded carrier forms, \(E_o\) and \(E_i\) (Stein, 1986). In contrast, the carrier described here exhibits substantial conductive Ca\(^{2+}\) flux due to slippage (Fig. 1, A and B) as well as Ca\(^{2+}\)–Ca\(^{2+}\) exchange (in cells loaded with 0.24 mM Ca\(^{2+}\); Fig. 5). Under physiologic conditions, the extremely low [Ca\(^{2+}\)], 20–30 nM (estimated in Lew et al., 1982), does not permit an exchange-only reaction cycle (compare the [Ca\(^{2+}\)], of 20–30 nM to the carrier's intrinsic dissociation constant, \(1/K_c^a\), of 0.68 mM). If physiologic Ca\(^{2+}\)–Ca\(^{2+}\) exchange were substantial, lowering [Ca\(^{2+}\)] would be expected to reduce \(^{45}\text{Ca}^{2+}\) influx. We found that exchange is negligible: subphysiologic [Ca\(^{2+}\)] (produced by chelator loading) did not reduce \(^{45}\text{Ca}^{2+}\) influx (Fig. 1 B). Thus, the carrier's physiologic mode of operation is net entry with almost no exchange.
APPENDIX

Unidirectional Hux Equations for the Simple Carrier of Scheme I

The most general Ca\(^{2+}\) flux equations for the carrier in Scheme 1 are:

\[ v_{in} = \frac{\overline{S}_1 + \exp(\mu u)\overline{S}_2 + \overline{S}_P}{[R_{so} + R_{12}\overline{S}_1 + \exp(\mu u)R_{21}\overline{S}_2 + \exp(-\mu u)R_{12}\overline{P}_1 + R_{21}\overline{P}_2 + R_{22}\overline{P}_2] + \exp[(\epsilon - \mu u)R_{22}\overline{S}_F + \exp(-\mu u)R_{22}\overline{P}_P] + \exp\left[(\mu - \mu u)R_{22}\overline{P}_P\right]} \]

\[ v_{out} = \frac{\exp(\mu u)\overline{S}_2 + \exp(-\mu u)\overline{P}_P}{[R_{so} + R_{12}\overline{S}_1 + \exp(\mu u)R_{21}\overline{S}_2 + \exp(-\mu u)R_{12}\overline{P}_1 + R_{21}\overline{P}_2 + R_{22}\overline{P}_2] + \exp[(\epsilon - \mu u)R_{22}\overline{S}_F + \exp(-\mu u)R_{22}\overline{P}_P] + \exp\left[(\mu - \mu u)R_{22}\overline{P}_P\right]} \]

where

\[ \overline{S}_1 = K^{\mu}[Ca^{2+}], \quad \overline{S}_2 = K^{\mu}[Ca^{2+}]. \]

\[ \overline{P}_1 = K^{\mu^*}[Sr^{2+}], \quad \overline{P}_2 = K^{\mu^*}[Sr^{2+}]. \]

\(K^\mu\) and \(K^{\mu^*}\) carrier's intrinsic affinities for Ca\(^{2+}\) and Sr\(^{2+}\)

\[
\begin{array}{|c|c|}
\hline
\text{Parameter} & \text{Expression} \\
\hline
K^\mu & \frac{f_c f_g}{1 + \frac{1}{k_1 + \frac{1}{k_2}}} \\
K^{\mu^*} & \frac{1}{1 + \frac{1}{1} + \frac{1}{h_2}} \\
E_{so} \times R_{so} & 1 \\
E_{so} \times R_{12} & \frac{1}{b_2 + \frac{1}{b_1 + \frac{1}{b_2 + \frac{1}{b_1 + \frac{1}{b_2 + \frac{1}{b_1 + \frac{1}{b_2}}}}}}}} \\
E_{so} \times R_{21} & \frac{1}{b_2 + \frac{1}{b_1 + \frac{1}{b_2 + \frac{1}{b_1 + \frac{1}{b_2 + \frac{1}{b_1 + \frac{1}{b_2}}}}}}}} \\
E_{so} \times R_{12} & \frac{1}{b_2 + \frac{1}{b_1 + \frac{1}{b_2 + \frac{1}{b_1 + \frac{1}{b_2 + \frac{1}{b_1 + \frac{1}{b_2}}}}}}}} \\
E_{so} \times R_{21} & \frac{1}{b_2 + \frac{1}{b_1 + \frac{1}{b_2 + \frac{1}{b_1 + \frac{1}{b_2 + \frac{1}{b_1 + \frac{1}{b_2}}}}}}}} \\
E_{so} \times R_{12} & \frac{1}{b_2 + \frac{1}{b_1 + \frac{1}{b_2 + \frac{1}{b_1 + \frac{1}{b_2 + \frac{1}{b_1 + \frac{1}{b_2}}}}}}}} \\
E_{so} \times R_{21} & \frac{1}{b_2 + \frac{1}{b_1 + \frac{1}{b_2 + \frac{1}{b_1 + \frac{1}{b_2 + \frac{1}{b_1 + \frac{1}{b_2}}}}}}}} \\
E_{so} \times R_{12} & \frac{1}{b_2 + \frac{1}{b_1 + \frac{1}{b_2 + \frac{1}{b_1 + \frac{1}{b_2 + \frac{1}{b_1 + \frac{1}{b_2}}}}}}}} \\
E_{so} \times R_{21} & \frac{1}{b_2 + \frac{1}{b_1 + \frac{1}{b_2 + \frac{1}{b_1 + \frac{1}{b_2 + \frac{1}{b_1 + \frac{1}{b_2}}}}}}}} \\
E_{so} \times R_{12} & \frac{1}{b_2 + \frac{1}{b_1 + \frac{1}{b_2 + \frac{1}{b_1 + \frac{1}{b_2 + \frac{1}{b_1 + \frac{1}{b_2}}}}}}}} \\
E_{so} \times R_{21} & \frac{1}{b_2 + \frac{1}{b_1 + \frac{1}{b_2 + \frac{1}{b_1 + \frac{1}{b_2 + \frac{1}{b_1 + \frac{1}{b_2}}}}}}}} \\
E_{so} \times R_{12} & \frac{1}{b_2 + \frac{1}{b_1 + \frac{1}{b_2 + \frac{1}{b_1 + \frac{1}{b_2 + \frac{1}{b_1 + \frac{1}{b_2}}}}}}}} \\
E_{so} \times R_{21} & \frac{1}{b_2 + \frac{1}{b_1 + \frac{1}{b_2 + \frac{1}{b_1 + \frac{1}{b_2 + \frac{1}{b_1 + \frac{1}{b_2}}}}}}}} \\
E_{so} \times R_{12} & \frac{1}{b_2 + \frac{1}{b_1 + \frac{1}{b_2 + \frac{1}{b_1 + \frac{1}{b_2 + \frac{1}{b_1 + \frac{1}{b_2}}}}}}}} \\
E_{so} \times R_{21} & \frac{1}{b_2 + \frac{1}{b_1 + \frac{1}{b_2 + \frac{1}{b_1 + \frac{1}{b_2 + \frac{1}{b_1 + \frac{1}{b_2}}}}}}}} \\
E_{so} \times R_{12} & \frac{1}{b_2 + \frac{1}{b_1 + \frac{1}{b_2 + \frac{1}{b_1 + \frac{1}{b_2 + \frac{1}{b_1 + \frac{1}{b_2}}}}}}}} \\
E_{so} \times R_{21} & \frac{1}{b_2 + \frac{1}{b_1 + \frac{1}{b_2 + \frac{1}{b_1 + \frac{1}{b_2 + \frac{1}{b_1 + \frac{1}{b_2}}}}}}}} \\
E_{so} \times R_{12} & \frac{1}{b_2 + \frac{1}{b_1 + \frac{1}{b_2 + \frac{1}{b_1 + \frac{1}{b_2 + \frac{1}{b_1 + \frac{1}{b_2}}}}}}}} \\
E_{so} \times R_{21} & \frac{1}{b_2 + \frac{1}{b_1 + \frac{1}{b_2 + \frac{1}{b_1 + \frac{1}{b_2 + \frac{1}{b_1 + \frac{1}{b_2}}}}}}}} \\
\hline
\end{array}
\]

The parameters in Eqs. A1 and A2 are obtained by regrouping terms in the derived unidirectional rate equations according to substrate concentrations. These are represented here by a notation similar to that suggested by Stein (1986). \(E_{so}\) represents the total concentration of the carrier (sum of all six forms in Scheme 1).
$R$ (with subscripts) resistance terms describing ease of interconversion between carrier inter-
mediates (notation of Stein, 1986)
z and $z_v$ valences of $S$ and $P$ ($Ca^{2+}$ and $Sr^{2+}$, respectively)

and

$$u = FV_m/RT$$

where

$F$ the Faraday

$V_m$ membrane potential

$R$ (no subscript) the gas constant

$T$ absolute temperature

The resistance terms ($R$'s with subscripts), $K_{Ca}$, and $K_{Sr}$ are functions of the 14 first-order rate
constants in Scheme 1, $z_s$ and $z_p$, and $u$, but not of the concentrations of $S$ or $P$. These functions
are given explicitly in Table I.

We thank Dr. Paul De Weer and Dr. Albert Roos for their help and advice.

These studies were supported by grant HL-12839 from the National Heart, Lung and Blood
Institute, grant AI-07172 from the National Institute of Allergy and Infectious Diseases, and grant
GMO-7200 from the National Institute of General Medical Sciences.

Original version received 9 July 1990 and accepted version received 4 January 1991.

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