Adaptive R-Peak Detection on Wearable ECG Sensors for High-Intensity Exercise

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Abstract—Objective: Continuous monitoring of biosignals via wearable sensors has quickly expanded in the medical and wellness fields. At rest, automatic detection of vital parameters is generally accurate. However, in conditions such as high-intensity exercise, sudden physiological changes occur to the signals, compromising the robustness of standard algorithms. Methods: Our method, called BayeSlope, is based on unsupervised learning, Bayesian filtering, and non-linear normalization to enhance and correctly detect the R peaks according to their expected positions in the ECG. Furthermore, as BayeSlope is computationally heavy and can drain the device battery quickly, we propose an online design that adapts its robustness to sudden physiological changes, and its complexity to the heterogeneous resources of modern embedded platforms. This method combines BayeSlope with a lightweight algorithm, executed in cores with different capabilities, to reduce the energy consumption while preserving the accuracy. Results: BayeSlope achieves an F1 score of 99.3% in experiments during intense cycling exercise with 20 subjects. Additionally, the online adaptive process achieves an F1 score of 99% across five different exercise intensities, with a total energy consumption of 1.55±0.54 mJ. Conclusion: We propose a highly accurate and robust method, and a complete energy-efficient implementation in a modern ultra-low-power embedded platform to improve R peak detection in challenging conditions, such as during high-intensity exercise. Significance: The experiments show that BayeSlope outperforms state-of-the-art QRS detectors up to 8.4% in F1 score, while our online adaptive method can reach energy savings up to 38.7% on modern heterogeneous wearable platforms.

I. INTRODUCTION

In recent years, increasing healthcare costs [1] and hospital overcrowding have pushed new technological advances to improve remote wellness monitoring, and enable early intervention and prevention [2]. In addition, population aging and the resulting higher incidence of noncommunicable diseases (NCDs) create the need for long-term health monitoring. For these reasons, there is an increasing demand for applications working on wearable platforms that continuously and remotely monitor biosignals, such as electrocardiogram (ECG) [3] or photoplethysmography (PPG), and extract relevant health parameters from them. Furthermore, daily physical activity is highly recommended [4] to prevent NCDs, and in particular high-intensity interval training (HIIT) are postulated as a good alternative to moderate intensity for health improvement [5].

As we illustrate in Section II, during intense physical exercise sudden physiological changes occur, such as short RR intervals, high breathing frequency and noise from respiratory sinus arrhythmia, or sympathetic activation, amongst others [6]. These changes induce artifacts or noise that are in general not properly detected by standard algorithms, leading to a need for using advanced computing techniques, such as machine learning and online adaptivity, to improve the robustness of the analysis. However, with the advancement of new complex algorithms comes the question of managing constrained resources in wearable sensor nodes (WSNs), and the consequent toll on energy consumption.

In fact, the implementation of complex biomedical applications in traditional WSNs can cause a significant draining of platform resources leading to frequent device charging [7]. Furthermore, various algorithmic optimizations implemented to lower the device energy consumption can lead to a decrease in the output accuracy of the algorithm [8]. With the advent of modern ultra-low power (ULP) platforms [9] and their capabilities, the trade-off between optimizing the device resources to lower the energy consumption and maintaining a highly accurate output has become more attainable [10], [11]. Nevertheless, in the context of complex biomedical applications for WSN-based wellness monitoring, the designer has to consider new challenges to achieve an optimal energy-accuracy trade-off. First,
in the acquired biosignals of various pathologies or physical conditions sudden events occur, which traditional algorithms can miss or misinterpret (e.g., atrial fibrillation (AF) or intense physical exercise) [6], [12]. For this reason, their robustness is compromised and severely affects the reliability of the wellness progress in the long term. Second, the static nature of traditional algorithms do not include the adaptive management of platform resources at run time according to the complexity of the application, which has recently become a need in WSNs design. New methods tackle self-aware applications at the algorithmic level applying a multi-layer classification or detection system with increasing complexity [13], [14]. Based on the confidence of the low complexity classifiers, the algorithm decides whether to execute a more complex layer and, therefore, consumes more energy. However, these methods are targeted to traditional homogeneous platforms, and some do not consider the error in the pathological events detection.

For the reasons above, in this work, we propose an online adaptive design of a new ECG R peak detection algorithm for wearable systems based on unsupervised machine learning, which exploits the capabilities and heterogeneity of modern ULP platforms. In the proposed design, we introduce for the first time BayeSlope, a slope-based R peak detector that applies a Bayesian filter, non-linear normalization, and a clustering technique to an ECG segment. In the literature, the use of slope-based QRS detectors has been extensive [15], [16]. There are examples of the use of the Kalman filter for smoothed estimation of the heart rate (HR), different than R peak detection, and using multiple signals [17]. However, many of these works target ambulatory monitoring. Hence, to the best of our knowledge, this is the first time that an R peak detection like BayeSlope is applied in the context of intense physical exercise. In fact, we test the proposed method with a dataset collected in collaboration with the Institut des sciences du sport de l’Université de Lausanne (ISSUL), where the subjects performed a maximal exercise test on a cycle ergometer till exhaustion. Our main contributions are:

- We propose a new highly accurate slope-based R peak detection method that is specifically aimed at high intensity exercise application scenarios. Our new R peak detection method, called BayeSlope, applies a Bayesian filter and a non-linear normalization to the input ECG signal. The combination of these signal processing techniques enhances and correctly detects the next R peak in the expected position on a peak-to-peak resolution. During high intensity exercise, BayeSlope outperforms the most popular state-of-the-art QRS detectors up to 8.4% in \( F_1 \) score, while being comparable during low intensity exercise.
- We pair the newly proposed algorithm with the REW ARD algorithm, presented in [18], which is less complex though more prone to error if sudden events occur. To ensure the adaptive nature of the design, we propose an error detection routine applied to REW ARD that triggers BayeSlope if REW ARD fails.
- To apply adaptive management of resources at run time according to the algorithm’s complexity, we implement the proposed method on an heterogeneous platform, that allows to run BayeSlope on a more capable core than the one where REW ARD runs, which is simpler. In fact, the R peak detection step of REW ARD is approximately 104 × less complex than BayeSlope when running on the same core. Hence, a simpler processor can handle it better, while a more powerful core handles better the more complex BayeSlope.
- The fully adaptive process has an \( F_1 \) score of up to 99.0%, comparable to always running BayeSlope, which achieves an \( F_1 \) score up to 99.3%, across five different exercise intensities. Moreover, our proposed adaptive process is up to 17.5% more accurate compared to running only REW ARD, across the five exercise intensities. Finally, the adaptive method tailored for modern heterogeneous platforms can reach energy savings up to 38.7% compared to continuously executing BayeSlope. Therefore, the newly proposed adaptive design is the best solution for an optimal energy-accuracy trade-off for long-term wellness monitoring with latest wearable systems.

In Section II, we describe what occurs during intense physical exercise and the relevance of a highly accurate R peak detection in such conditions. In Section III, we present the new R peak detection algorithm and its adaptive design. In Section IV, we describe the protocol of the experiments and the platform used. Finally, in Sections V and VI, we present, respectively, the results and the conclusion of our analysis.

II. BACKGROUND

To motivate the newly proposed method for autonomous wellness monitoring, let us consider the sudden changes occurring in the ECG during intense physical exercise. We will focus specifically on the R peak, as it is the basis for ECG analysis. Fig. 1 shows two segments of ECG acquired from a subject performing a maximal exercise test (c.f. Section IV). The segments were extracted from the initial rest condition (Fig. 1a) and a window of intense physical exercise, close to exhaustion (Fig. 1b). As shown in Fig. 1b, the peak-to-peak (RR) interval variability is significantly low compared to a rest condition. Moreover, the amplitude of the R peaks is highly variable. Therefore, when standard algorithms are used to detect the peaks in these conditions, their robustness is compromised. In this work, we consider one R peak detection algorithm that was presented in [18], called REW ARD, as the standard base algorithm to build on and motivate our proposed online adaptive method. REW ARD can detect peaks within a window of 1.75 s by adapting hysteresis thresholds based on the average and maximum (or minimum if R is negative) amplitude of the peaks within a window. This method works well when the amplitude variability is limited, as shown in Section V-A. However, during intense physical exercise, the RR interval decreases significantly and the amplitude highly varies between one peak and the other—within 1.75 s, there are many peaks significantly different in amplitude—with the result that REW ARD fails to detect smaller peaks. In Fig. 3, we show an example of an ECG segment extracted from the analyzed dataset and, specifically, a window where REW ARD fails.
Fig. 1. Effects of intense physical exercise on ECG, and, specifically, the R peak amplitudes and RR interval variability, compared to rest. The ECG segments are extracted from the database presented in Section IV. Specifically, the segment in Fig. 1a is extracted from the first 3 min of rest of the maximal exercise test of Subject 3, starting at second nine. The segment in Fig. 1b is extracted close to exhaustion of Subject 3 during the maximal exercise test, starting at approximately 27 min. (a) Rest. (b) Intense physical exercise.

To capture the changes occurring during various intensities of physical exercise in the wellness context, there exists a gold standard protocol where subjects perform a maximal exercise test on a cycle ergometer or a treadmill till exhaustion. The subjects wear a gas mask that measures the volume of O\textsubscript{2} and CO\textsubscript{2} (VO\textsubscript{2}, VCO\textsubscript{2}) inhaled and exhaled [19]. Additionally, the protocol includes the acquisition and analysis of a single-lead ECG, from which specific heart rate variability (HRV) parameters can be extracted to help in the estimation of the so-called ventilatory thresholds (VT1, VT2) [20], and VO\textsubscript{2} max [21]. These three variables describe the cardiovascular and respiratory state during intense physical exercise. VT1 measures the hyperpnea (i.e., faster breathing) caused by the increased production of CO\textsubscript{2} for exercise intensities above the anaerobic threshold resulting in a non-linear increase in the ratio between ventilatory flow (VE) and VO\textsubscript{2}. VT2 represents a phase where the hyperpnea is not enough to eliminate the CO\textsubscript{2}, which remains constant, leading to a sharp increase of VE/VCO\textsubscript{2}. Finally, VO\textsubscript{2} max is the final stage where exhaustion is reached and, consequently, a maximum oxygen uptake and HR. The determination of the ventilatory thresholds usually relies on an agreement between medical experts who evaluate the gas analysis and the HRV parameters to find the position of the thresholds [22].

The HRV analysis uses the RR time series of an ECG signal to extract time and frequency domain features, which can be used for a direct estimation of VT1, VT2 and VO\textsubscript{2} max [20]. The current methods for this estimation are performed in post-processing with the help of medical experts and, usually, require interpolation and correction of the RR time series. The R peak detection needs to be accurate, robust and adapt at run time to sudden changes to ensure the correct comparison between ventilatory measurements and the RR time series. Therefore, we propose BayeSlope, a new highly accurate and robust R peak detection algorithm for wearable sensors, which is paired to REWARD. BayeSlope is much more complex than REWARD, and, if run continuously, it can drain the device battery. For this reason, we additionally propose a real-time strategy that automatically adapts the algorithm’s complexity and the resources assigned based on the robustness of REWARD, for an enhanced energy-accuracy trade-off in latest ultra-low power autonomous wearable systems.

III. ADAPTIVE R PEAK DETECTION IN MODERN WEARABLE SENSORS

One of the main problems in the context of edge computing in WSNs is minimizing energy consumption while maximizing output accuracy. In this section, we describe our proposed method to detect R peaks from a single-lead ECG that optimizes the energy-accuracy trade-off with a two-level adaptive method. Fig. 2 shows the data-flow diagram of the full process and the architecture where the algorithm is implemented [9]. The two-level adaptivity consists in the robustness and complexity of the two different R peak detection algorithms, namely REWARD [18] and BayeSlope. As described in Section II, REWARD uses hysteresis thresholds that are adapted to each
A standard R peak detection algorithm requires several steps of preprocessing of the ECG input signal. In this case, the input is a single-lead ECG where a morphological filtering (MF) is applied to remove the baseline and high frequency noise [23]. Then, the signal is enhanced by applying the Relative-Energy (Rel-En) method, which amplifies the most dominant peaks [18]. This preprocessing method is part of the REWARD algorithm presented in [18]. The second part of the algorithm searches for the R peak in a window of 1.75 s using hysteresis thresholds based on the ECG morphology within the window. However, during intense physical exercise, the interval between two R peaks (i.e., RR interval) decreases significantly and sudden changes in amplitude occur. Therefore, within a window of analysis, many peaks can be missed, as shown in Fig. 3. Moreover, right after exhaustion during a maximal exercise test, there can be an increase of the T wave amplitude—the wave after the QRS complex that represents the repolarization of the heart ventricles—often significantly more dominant than the R peak itself, and a decrease of the RT interval. In these conditions, REWARD fails in detecting very small peaks as the hysteresis thresholds are skewed by the higher amplitude variability of the peaks within the window. However, it performs extremely well if these events do not occur as demonstrated in [18].

For this reason, we propose a statistical method to identify potential errors in the R peak detection within a window of 1.75 s by analyzing the distribution of the ratio $\frac{RR(n)}{RR(n-1)}$, where $n = 0, 1, 2, \ldots$, of all the data acquired. This distribution has been computed offline using the results of BayeSlope, since it is the most accurate (c.f., Section V). However, to avoid data snooping, for each subject, the RR ratio distribution is computed with a leave-one-out (LOO) strategy, in which the analyzed subject is not included in the distribution. The RR ratio can capture sudden changes with a three-peak resolution, such as missing peaks, additional wrong peaks (e.g., T wave), and highly noisy signal segments. We want to underline that the main objective of the error detection mechanism is to balance the execution of REWARD and BayeSlope to optimize the energy consumption. Thus, this mechanism has a marginal influence on the R peak detection accuracy. There is only one situation, thoroughly explained in Section V, in which a mistake in the error detection can lead to misdetected peaks.

First, the method computes offline the RR intervals and the corresponding RR ratio sequence used for the distribution from all the subjects, except the one that is being analyzed. Then, for each subject, if at least one value of RR ratio computed within each window falls in the tails of the distribution (below the 0.5 or above the 99.5 percentiles of the RR ratio distribution, respectively), the algorithm detects an error. This is performed in the online phase of the error detection applied to the output...
Algorithm 1: BayeSlope R Peak Detection.

1: Input: windows of RelEn signal, $s$ ($\mu V$)
2: Output: R peaks, $r$
3: Initialize centroids: $hcentr = \text{percentile}(\text{diff}(s), 99)$ and $lcentr = 1$
4: $min_{rr\_dist} = 240$ ms; $max_{qrs\_dur} = 140$ ms; $\triangleright$ Constant parameters
5: Initialize: $mu = 75$ bpm; $sd = 100$ ms; $zeroctr = 0$; $qrs\_init = 0$; label = 0; in_qrs = false;
6: for $i = 2, \ldots \text{length}(s)$ do
7: $s2[i] = s[i] - s[i - 1]$; $\triangleright$ Derivative approximation
8: $x = \text{abs}(s2[i])$
9: $bf[i] = \text{gaussian}(i - \text{last\_peak}, mu, sd)$; $\triangleright$ Bayesian filter
10: $bt[i] = \text{genlogfun}(x, \text{param\_logfun})$; $\triangleright$ Sigmoid normalization
11: $st[i] = \max(x, bt[i] + bf[i])$; $\triangleright$ Normalize signal
12: Update $hcentr$ and $lcentr$ each as the new mean of their cluster
13: if in_qrs then $\triangleright$ Peak search
14: if label = 0 then
15: $zeroctr += 1$
16: else
17: $zeroctr = 0$
18: end if
19: if zeroctr = 30 OR $i > last\_peak + min_{rr\_dist}$ then
20: $max_{min\_slope} = \text{argmaxmin}(st * \text{sign}(s2))$
21: Search for new peak within $max_{min\_slope}$
22: $r[i] = \text{new\_peak}$
23: end if
24: else
25: if label = 1 AND $i > \text{last\_peak} + min_{rr\_dist}$ then
26: in_qrs = true;
27: $qrs\_init = i$
28: end if
29: end if
30: end for

Even though the distributions are different, the standard deviation among the subjects is quite small, suggesting that the RR ratio has a low inter-patient variability. On the other hand, the range of the distribution suggests a high intra-patient variability. Considering these values of thresholds, Fig. 4 shows shadowed areas in grey, which represent the range of RR ratio for which an error is detected. Moreover, this figure shows a light green area that represents the range of RR ratio for which no error in the R peaks exists. Finally, the darker grey areas and the vertical lines represent the full range of percentile thresholds reported in (1). Therefore, if we consider the ECG example in Fig. 3, the error detection results are shown in Fig. 5, where the values of the RR ratio over the segment are reported. Considering the percentile thresholds $P_{0.5} = 0.64$ and $P_{99.5} = 1.47$ for the analyzed subject, the method can detect an error where REWARD fails. The last peak in Fig. 3 where there is an error would be detected in the next window. It is worth mentioning that there are genuine physiological events, such as ectopic heartbeats, that can cause a variation in the RR ratio in the tails of the distribution, and therefore they will be detected as “errors”. These events will lead to trigger the BayeSlope algorithm, but it does not mean that they will be ignored or undetected, as long as they fit the detection conditions of BayeSlope.

### B. BayeSlope: Adaptive Slope-Based R Peak Detection

Once an error is detected, a more accurate adaptive R peak detection, BayeSlope, is triggered. This newly proposed method applies a non-linear normalization of the signal and a Bayesian filter to enhance high slope areas which are near the expected position of the next peak according to the current HR. These high slope areas are assumed to belong to the QRS complex, and to distinguish them from low slope areas, the approach relies on a clustering method based on K-means.

Algorithm 1 describes the main steps of BayeSlope. The method takes as input the Rel-En signal window, $s$, and it outputs the vector of R peaks detected. The algorithm is derivative-based, and considers two clusters that represent the high and low slope areas of the signal. Then, the two centroids are initialized beforehand, as shown in Line 3, where $hcentr$ is the $99^{th}$ percentile of the derivative of $s$ and $lcentr = 1$. When a new sample is assigned to a cluster it is labeled as 1 if it is closer to $hcentr$, or 0 if it is closer to $lcentr$. Two windows of 1.75 s. 

**Fig. 5.** Result of error detection on example ECG extracted from Subject 3 of the dataset used (c.f., Section IV-A). The values of the RR ratio are computed on a resolution of three R peaks. Considering the percentile thresholds for the analyzed subject (bottom left), the method can detect an error where REWARD fails (in the red boxes).

$P_{0.5} = 0.64$ $P_{99.5} = 1.47$
are used for the $hectr$ initialization to account for enough peaks even at rest and avoid errors due to signal noise. Then, the algorithm initializes all the other parameters needed, constant and varying, in Lines 4–5. The values for these parameters were chosen based on common physiological constraints [24], and not on any values observed in the data. Thus, we can be confident that the values are general enough for any ECG obtained from an adult human.

The main process starts by considering the derivative of $s$ and computing its absolute value, $x$, in Lines 7–8. We apply this initial transformation to enhance the maximum and minimum slopes of the original signal $s$. This choice follows the assumption that the R peak is located in general within the maximum upward and downward deflections within an ECG signal. Next, the method computes the Bayesian filter (Line 9), which is a Gaussian centered on the expected peak, $\mu$, with standard deviation $sd$, two parameters computed based on the last five peaks. The selection of such a small number of peaks is to make the Bayesian filter responsive to the potential fast variations of the RR interval near high intensity limits [25], which are precisely the regions of greatest interest to our algorithm. Then, in Line 10, the algorithm computes the generalized logistic function [26] with input $x$ and its parameters computed based on the last $hectr$ and $lcentr$. The sigmoid varies between 0 and the value of the higher k-means centroid, $hcentr$. The sigmoid and the Bayesian filter are used to normalize the peak or, specifically, to increase the amplitude of expected small peaks, as shown in Line 11 and Fig. 6. If the analyzed sample does not reach the computed threshold, the function does not increase its value. When the input is approximately double the value of the lowest centroid, $st$ (in Algorithm 1) reaches the threshold between $lcentr$ and $hectr$, which determines the value of $label$. In Fig. 6, the expected location of the peak (i.e., the prior expectation) is depicted with the Gaussian centered on it. In this case, the original peak (i.e., observed value) in $x$ is small, and it is enhanced by the Gaussian multiplied by the sigmoid function, leading to the posterior estimation $st$. This situation is shown in the posterior estimation rectangle.

Once the signal is normalized, the algorithm starts a peak search within a QRS complex—the ECG main wave—in Lines 13–29. This procedure is also illustrated in Fig. 6. The distance between QRS complexes must be more than $min_{rr\_dist}$, according to standard physiological characteristics and the sample that starts the QRS complex ($qrs\_init$ in Line 25) must belong to the cluster represented by $hcentr$ (i.e., $label = 1$). Within the QRS complex, the algorithm waits till it reaches its maximum duration according to physiology ($max_{qrs\_dur}$) or for enough samples ($zeroctr = 30$) labeled 0 that represent the end of the QRS complex (Lines 14–19). Once within this interval (Lines 20–22), the algorithm computes the maximum and minimum of the function $st * sign(s2)$ representing the maximum upslope and downslope of the original signal. The sign function is used in case these values fall in the Q, S or T wave, which are not distinguished if only $st$ is used, as it is positive by definition. Finally, the $new\_peak$ is found and stored in the vector $r$.

C. Adaptive Design in Modern Heterogeneous Platforms

As shown in Fig. 2, the modules of the algorithm run in different cores of the wearable computing architecture according to the complexity of the corresponding module. The wearable architecture used in this work is based on one of the evolutions of the open-source PULP platform [27], called Mr.Wolf [9]. The PULP structure consists of a main streamlined processor, the fabric controller (FC), and an 8-core parallel compute cluster (CL). Moreover, PULP includes a direct memory access (DMA) that can transfer data to a multi-banked 512 KiB L2 memory during acquisition time or from L2 to a shared multi-banked 64 KiB L1 memory, which has a single-cycle latency in the cluster side. Both FC and CL are power-gated while the DMA fills the required L2 memory bank during sample acquisition. The FC is clock-gated when the CL is active, and each of the cores in the CL can be independently clock-gated to reduce dynamic power. Mr.Wolf includes a core for the FC (Zero-riscy) that is simpler than the RISCY cores of the CL, but it has a lower IPC. On the other hand, the cores of the CL have more
capabilities [28]. Therefore, this work considers the Mr.Wolf architecture by selectively using the FC and one core of the CL.

Considering this design, the modules of preprocessing (MF), REWARD (which includes Rel-En and R peak detection via hysteresis thresholds), and error detection run in the FC. REWARD is a very lightweight integer-based algorithm, as demonstrated in [18]. In a preliminary analysis, considering the dataset (c.f., Section IV-A), we performed a test executing the R peak detection step of REWARD on the FC and on one core of CL. The algorithm executed on CL is 1.23 × slower (in terms of execution time) and consumes 1.35 × more energy. Therefore, REWARD benefits from running on the FC, which is a simpler core, clocked at a higher frequency (170 MHz vs. 110 MHz of the CL). On the contrary, BayeSlope is about 100 × more complex than REWARD, hence, it benefits from running on a more advanced core with higher IPC. This helps to meet real-time constraints and limits the amount of time the system is active. Additionally, the Gaussian and the generalized logistic function of BayeSlope are implemented in floating-point. Since the FC does not have a floating-point unit, BayeSlope should be converted to fixed-point representation. Therefore, we adapted these functions of BayeSlope to employ fixed-point arithmetic, using a 32-bit representation with 1 sign bit, 15 integer bits, and 16 decimal bits. The results reveal that during the clustering step the algorithm quickly reaches the maximum range representable (i.e., approximately within 15 s of signal processing), with a consequent drop in accuracy. In contrast, this does not occur in the 32-bit floating-point representation as the maximum range is reached after approximately 27 h of signal processing. Therefore, we decided to implement BayeSlope on one core of the CL (RI5CY), which has a floating point unit and higher IPC.

After the signal filtering and REWARD running on the FC, the error detection (also running on the FC) checks the accuracy of the R peaks output. If an error is detected, the DMA transfers the necessary buffer of data from L2 to L1 ready for the core in the CL. Conversely, the FC is clock-gated. Since BayeSlope needs an initialization of the R peaks of two windows of 1.75 s, the previous window error needs to be checked. If the error in the previous window is 0, then the DMA transfers two windows, otherwise it transfers only one. This is an optimization applied in case REWARD fails more frequently and to avoid recomputing the same window. BayeSlope runs on the CL while the FC is clock-gated. The final output is the combination of correct R peaks from REWARD and BayeSlope. The full code for the adaptive R peak detection has been published as open-source software\(^1\).

IV. EXPERIMENTAL SETUP

A. Database Acquisition Protocol

The database was acquired considering 22 subjects performing an incremental test to exhaustion on a cycle ergometer for an average of 30 minutes each until VO\(_2\) max was reached, plus at least 1 minute post-exercise. The power of the cycle ergometer was increased every 3 min by 30 W, after initial 3 min of rest.

Moreover, a three-minute recovery period was recorded right after exhaustion. A single-lead ECG sampled at 500 Hz was acquired using the BIOPAC system [29], together with other biosignals and oxygen uptake measurements that were not used for this work. Fig. 7 shows a sketch of the positioning of biosignals sensors and the equipment used. The protocol was ethically approved by the Commission Cantonale (VD) d’Éthique de la Recherche sur l’Etre Humain (CER-VD), with reference 2016-00308, on 01/03/2018. For the experiments, the ECG was downsampled to 250 Hz since REWARD was validated only for this frequency in [18]. Two of the 22 subjects were discarded because one did not complete the protocol and for the second one the majority of the recording was corrupted. Therefore, the statistics and analysis were performed on 20 subjects. Next, five 20-second segments were extracted from the full ECG of each subject to be manually annotated by experts. The 20-second duration has been selected as a minimum to enable posterior HRV analysis [20]. The annotations were initially made by an engineer with background on ECG analysis, and then individually assessed by a cardiologist. A consensus was achieved among both annotators after just one iteration. The annotation process was done on PDF files with the standard ECG grid of 0.2 s × 0.5 mV, as shown in Fig. 10. The segments were chosen based on the different phases of the maximal exercise test, namely, considering higher intensities of exercises where it is more likely that sudden changes occur. Then, these segments were extracted and reported in the order shown in Fig. 8: the first, 30 s before VT2; the second, 60 s after VT2; the third, 30 s before VO\(_2\) max (exhaustion); the fourth, at the moment of exhaustion (centered in VO\(_2\) max); finally, the fifth, 60 s after VO\(_2\) max, i.e. during the recovery after exhaustion. The segments at rest were ignored since REWARD performs very well in this condition, and there is no need to

\(^1\)https://c4science.ch/source/adaptive_rpeak_det_public
run BayeSlope. Moreover, also the segments near VT1 are not considered as they represent lower intensities of exercise for which the performance of REWARD is satisfactory. Only one out of 100 segments was not extracted and annotated (subject 9, segment during recovery). In fact, the recording for this subject was stopped right after exhaustion (instead of after three minutes of recovery expected by the protocol) and it was not possible to have a 20-second segment 60 s after VO\textsubscript{2} max. The input segments to the peak detection were extracted considering the 20 s given to the experts and going backward of 0.6 s + 0.95 s + 1.75 s, which represents, respectively, the initial delay of the MF, the initial delay of Rel-En, and one additional window of analysis for BayeSlope initialization; and going forward 1.75 s to avoid missing the last peaks. Thus, each segment is approximately 25 s long. The accuracy of R peak detection is measured according to the standard tolerance of 150 ms between the detected peaks and the manual annotations [30]. We also report for each subject the mean and standard deviation of the time difference between the two. We first compare the accuracy of BayeSlope against a broad spectrum of state-of-the-art methods, including:

1) The Pan-Tompkins algorithm [31], which is the most widely used QRS detector in the literature. It is based on a combination of bandpass filtering and differentiation.
2) A variation of the Engelse-Zeelenberg (EngZee) method, which is based on a heavy difference filter and which is considered particularly robust to noise and artifacts [32].
3) The GQRS detector [33], which belongs to the matched-filter family of methods.
4) A more modern method based on adaptive thresholding on the Stationary Wavelet Transform (SWT) of the ECG [34].

We believe these four methods give a fair and complete overview of the different families of approaches that are typically used in embedded implementations. All the experiments were done with open-source implementations of the algorithms (specifically, [33] for GQRS and [35] for the other methods). Then, we also compare the accuracy of our algorithms in the following three designs:

a) Preprocessing (MF) and always running REWARD (Rel-En + peak detection);
b) Preprocessing (MF + Rel-En) and always running the newly proposed BayeSlope;
c) Our proposed adaptive design including preprocessing (MF), REWARD (Rel-En + peak detection), error detection and running BayeSlope only when REWARD fails.

All the segments used in the experiments, as well as the manual annotations, have been published as an open dataset [36].

B. Test Benches on the Heterogeneous Platform

The three designs are mapped on the Mr.Wolf platform to estimate their overall energy consumption and perform the energy-accuracy analysis. In all test benches, the preprocessing always runs on the FC. The first two test benches consist of 1) REWARD running on the FC with the CL power-gated, and 2) BayeSlope always running on the CL. The third test bench consists of the fully adaptive process, including the error detection, with REWARD running on the FC and BayeSlope running on CL when REWARD fails. Each of the test benches is applied to the 99 segments described in Section IV-A.

To measure the execution time of the three configurations, we used the open PULP platform [27]. PULP provides an SDK to run RTL simulations, using Modelsim, in order to obtain a cycle-accurate profiling. To estimate the energy consumption of our proposed system, we use the power numbers reported for a chip based on the PULP architecture implemented in TSMC 40 nm LP CMOS technology, namely, Mr.Wolf [9]. We consider the lowest energy point of the platform, at 0.8 V. The platform requires 3.6 \mu W [37] when power-gated\textsuperscript{2} and 12.6 \mu W with full L2 retention. To implement better memory management of the activated banks as done in [38], we reduce the L2 to 128 KiB, with a resolution of 16 KiB per memory bank, since the application does not need more memory. When the System-on-Chip (SoC) architecture of PULP is active, it consumes 0.98 mW with its main processor clock-gated, and 6.66 mW while operating at 170 MHz. Once the CL is activated, it consumes 0.61 mW with all the cores clock-gated and 18.87 mW with the eight cores running at 110 MHz.

The three designs are compared first in terms of accuracy, then energy consumption of their mapping on Mr.Wolf, and then in their energy-accuracy trade-off for all the subjects and as a summary for worst, average and best cases.

V. EXPERIMENTAL RESULTS

A. Accuracy Analysis of the Test Benches

In Fig. 9, we report the percent of the error rate (ErrRate\%) in the peak detection of the three designs, described in Section IV-A, and its evolution through the type of segments for three example subjects. These examples illustrate three cases within the worst, best, and average groups in terms of accuracy of the new algorithm, BayeSlope, and the fully adaptive design (REWARD + Error detection (ErrDet) + BayeSlope) compared to REWARD. ErrRate\% is computed as \(1 - F_1\)*100, where \(F_1\) score measures the peak detection performance as:

\[
F_1 = \frac{TP}{TP + \frac{1}{2} \cdot (FP + FN)} \tag{2}
\]

where TP is the set of the correctly detected peaks that match the manual annotations. FN represents all the misdected peaks by the algorithm. FP is the set of all the peaks in the algorithm that do not match any manual annotation. The different segments shown in Fig. 9 represent increasing exercise intensities till the recovery after exhaustion (segment 5), as described in Section IV. In Fig. 9a, Subject 7 has one of the worst error rates for the new algorithm, and the reason is that segment 3 is quite noisy. The quality of the segment is shown in Fig. 10, where the amplitude of the ECG has a high variability due to changes caused by the exercise intensities near exhaustion (segment 3 is before VO\textsubscript{2} max). However, BayeSlope and its adaptive design, with an \(F_1\)

\textsuperscript{2}As reported for GAP-8 [37], which is an industrial version of PULP with state-of-the-art deep sleep optimizations not yet included in Mr.Wolf, its academic counterpart.
Fig. 9. Percent error rate with respect to the manual annotations of the three designs described in Section IV-A, for the worst, average, and best case subjects along five segments of increasing exercise intensities. (a) Worst case. (b) Average case. (c) Best case.

|        | Before VT2 | After VT2 | Before \( \overline{V}_{O_2} \) max | \( \overline{V}_{O_2} \) max | Recovery | Total |
|--------|------------|-----------|------------------------------------|-----------------------------|----------|-------|
| F\(_1\) (%) | REWARD (RW) | 92.1 | 90.9 | 78.7 | 80.2 | 92.5 | 86.7 |
|        | BayesSlope (BS) | 99.0 | 99.1 | 97.9 | 98.8 | 99.3 | 98.8 |
|        | BW + EntDet + BS | 98.9 | 99.0 | 96.2 | 97.1 | 98.5 | 97.9 |
| PPV (%) | REWARD (RW) | 98.2 | 98.2 | 97.1 | 96.3 | 98.1 | 97.6 |
|        | BayesSlope (BS) | 98.6 | 98.6 | 98.9 | 98.6 | 98.6 | 98.7 |
|        | BW + EntDet + BS | 98.3 | 98.4 | 97.3 | 96.2 | 97.5 | 97.5 |
| Sensitivity (%) | REWARD (RW) | 93.3 | 92.2 | 77.9 | 75.6 | 94.7 | 86.1 |
|        | BayesSlope (BS) | 96.0 | 95.7 | 80.4 | 83.4 | 97.2 | 91.6 |
|        | BW + EntDet + BS | 94.0 | 94.8 | 80.6 | 79.4 | 94.8 | 88.2 |

Table I: \( F_1 \) Score, PPV, Sensitivity (%) for the Three Test Benches and the Five Exercise Intensities Computed Across the Subjects

In Fig. 9b, Subject 3 represents an average case where REWARD has a lower error rate compared to the worst case (Subject 7), though still significant. In fact, the adaptive design performs significantly better, with an error rate up to 3%, slightly worse than BayesSlope. In Fig. 9c, Subject 16 is one of the best cases where REWARD fails only during more intense exercise (at exhaustion), with an error rate up to 5.5%, while BayesSlope has an error rate of only 1%.

Considering the five exercise intensities, a relevant summary of the algorithms’ performance is depicted in Table I. Here, we report the \( F_1 \) score, sensitivity, and positive predictive value (PPV) of the four reference algorithms and the three test benches for each of the five types of segment computed across the subjects, as well as the mean and standard deviation of the time difference between each test bench output and the manual annotations. Our results show that BayesSlope is the most accurate of the three designs over all the performance parameters. In particular, in comparison with state-of-the-art algorithms, only GQRS achieves a comparable \( F_1 \) score during lower intensity exercises, while BayesSlope is superior to all the compared methods in the rest of the situations. We can see that the main benefit of our proposal comes from an increased sensitivity during intense physical exercise (before and after \( \overline{V}_{O_2} \) max), which is precisely
the primary flaw observed in the other methods. This supports our starting hypothesis, according to which general algorithms are not suited to handle the artifacts and sudden changes in the ECG arising from intense exercise. Indeed, the $F_1$ score and the sensitivity of REWARD during intense exercise are below acceptable medical standards, compared to less intense exercise. However, combining both methods in an adaptive design is as accurate as BayeSlope (up to 1.7% of difference in $F_1$ score).

Rarely, the adaptive design could perform better (less than 1% difference in score) as it is shown in the sensitivity values. This is due to the initialization process of BayeSlope, which requires the signal to be stable as it does not use any prior information within this initial stage. Therefore, it happens rarely that the signal is more stable later in the segment where BayeSlope is triggered and will be initialized, compared to the initialization at the beginning of the segment (when always running BayeSlope). This can also cause a delay in the adaptation and very few peaks missed and result instead in a slightly worse accuracy. Another reason for a lower performance in the adaptive design compared to always running BayeSlope, specifically for intense exercise (before and after VO\textsubscript{2} max) and during recovery, as shown in Table I, is due to an edge case in the error detection. In fact, the RR ratio distribution used to compute the tail thresholds is performed on the full dataset and accounting for different exercise intensities. Within more intense exercises, as the RR intervals get smaller, it can happen that even if REWARD misses one peak, the RR ratio is still within the distribution. This is shown in Fig. 11, where the RR ratio computed on the small peaks not detected by REWARD is close to the $P_{99.5}$ of the distribution but not enough to trigger an error. In conclusion, the accuracy results show that always running BayeSlope is the most accurate and robust of the three designs. At the same time, REWARD’s performance highly varies with the intensity of the exercise. However, BayeSlope is approximately 100× more complex than the R peak detection step of REWARD. Therefore, we propose the adaptive design that combines both algorithms and has a similar accuracy compared to BayeSlope. In the next section, we will show the advantages in terms of energy consumption of the adaptive design on the PULP platform.

### B. Energy Consumption of Test Benches in PULP

Fig. 12 shows the energy consumption of the platform for the three subjects described in Section V-A. In Subject 7 (Fig. 12a), the worst case scenario, the fully adaptive design consumes the same amount of energy in almost all the windows. In segment 3, the adaptive design achieves 6.5% of energy savings compared to always running BayeSlope, with a 3.7% difference in $F_1$ score. However, the overall accuracy is far from the required medical standard, and even the best-performing state-of-the-art algorithms only reach 75%. In Subject 3 (Fig. 12b), for all the exercise intensities except segment 4, during exhaustion, the fully adaptive wearable design we propose has energy savings up to 48% compared to BayeSlope with a loss in accuracy of only up to 2% (c.f., Fig. 9b). For segment 3, even if the energy savings are one of the lowest at approximately 3.3%, the fully adaptive design is as accurate as BayeSlope and 18.8% more accurate compared to REWARD. Therefore, on average cases such as Subject 3, in most exercise intensities, choosing the fully adaptive design can improve the energy-accuracy trade-off. Subject 16, representing one of the best case scenarios in Fig. 12c, highlights the adaptivity of the full design and its error detection through the segments, starting with a minimum energy consumption, since only REWARD is running, and maximum attainable accuracy. Then, when the exercise intensity increases, REWARD fails more frequently, and BayeSlope takes over the R peak detection. Finally, during recovery, when the ECG stabilizes and REWARD fails less compared to exhaustion, the energy consumption drops to a lower level. Our fully adaptive design maintains a high level of accuracy (approximately 99%), while limiting the energy consumption compared to executing BayeSlope for the full segment, with energy savings from 31.8% up to 58.6%.

Fig. 13 shows how many times BayeSlope runs in the adaptive design in terms of percentage of windows over the full segment for the three cases analyzed. Considering the windows where an error occurs and triggers BayeSlope, the previous window also counts as triggered since BayeSlope needs an additional window for the initialization process (c.f., Section III-C). As expected, the trend is similar to the energy reduction compared to always running BayeSlope shown in Fig. 12. The large differences between the three subjects show how the proposed design can adapt to the subject and different exercise intensities to reduce energy consumption instead of constantly failing in the worst case scenario. This personalized and adaptive reduction...
Fig. 12. Energy consumption of the test benches described in Section IV-B for the worst, average, and best case subjects along five segments corresponding to increasing exercise intensities. (a) Worst case. (b) Average case. (c) Best case.

Fig. 13. Percentage of windows over the full segment where BayeSlope is triggered during the adaptive design for three worst, average, and best case scenarios. Comparing these trends with the ones shown in Fig. 12, it is evident that the adaptive design reduces energy consumption by reducing the number of times BayeSlope runs on the CL.

Table II

| Energy Consumption in MJ for the Three Test Benches and the Five Exercise Intensities Computed Across the Subjects | REWARD (RW) | BayeSlope (BS) | RW + ENSDet + BS |
|---------------------------------------------------------------|--------------|----------------|-------------------|
| Before VT2                                                   | 0.479±0.004  | 2.078±0.016    | 1.348±0.573       |
| After VT2                                                    | 0.479±0.003  | 2.070±0.032    | 1.469±0.556       |
| Before VO_{2}\text{max}                                     | 0.476±0.004  | 2.071±0.037    | 1.840±0.299       |
| VO_{2}\text{max}                                            | 0.476±0.003  | 2.075±0.032    | 1.820±0.409       |
| Recovery                                                     | 0.477±0.002  | 2.080±0.020    | 1.275±0.562       |
| Total                                                        | 0.477±0.004  | 2.075±0.028    | 1.553±0.536       |

TABLE II

The adaptive design reduces energy consumption by reducing the number of times BayeSlope runs on the CL. The power of the platform corresponds to the power of the FC and the leakage power of the CL, which is significantly lower (approximately $5 \times$) than the power of the CL executing BayeSlope on one of its cores, with the other ones clock-gated. Therefore, the energy consumption over the 25-second segment is reduced. As a result, the adaptive design achieves energy savings up to 38.7%, considering the average for the five exercise intensities. Moreover, it reaches up to 74.2% energy savings for the overall dataset analyzed, compared to the scenario where the CL is always active and executes BayeSlope.

C. Energy-Accuracy Trade-Off on Test Benches

Fig. 14 shows the energy-accuracy comparison between the three test benches and an analysis on the different exercise intensities. We use once again the $F_1$ score as a measure of algorithm detection accuracy. For the three segments before and after VT2, and during the recovery after VO_{2}\text{max}, REWARD is accurate within the medical acceptability, and consumes the minimum energy for this application. However, the fully adaptive design (in purple) is always more advantageous in terms of accuracy, with a performance increase of up to 8.2%. Moreover, it is comparable in $F_1$ score to BayeSlope although more energy-efficient, with energy savings up to 38.7%.

However, when the exercise intensity increases, the number of peaks within a window increases as well. In this condition, the hysteresis thresholds of REWARD do not adapt to the high
amplitude variability of the peaks within a window of analysis (1.75 s), as described in Section III-A and Fig. 3. In fact, before VO2 max the exercise intensity is about to reach its maximum, and more sudden changes in the ECG occur, which explains the decreased accuracy of REWARD. The segment extracted during exhaustion (i.e., when reaching VO2 max) represents the highest intensity and, hence, disruption of the ECG morphology, specifically in the amplitude of the R peak and the RR intervals (HRV reaches its minimum). Therefore, it is the reason for a decreased performance in REWARD. On the contrary, the F1 score of the fully adaptive design is only up to 1.7% lower than BayeSlope, which is the most accurate. The energy savings for these two segments are lower than the other three, though still significant (up to 12.2%).

Our experimental results show how the proposed BayeSlope algorithm is highly accurate and more robust than the lightweight REWARD when sudden changes in the ECG morphology occur. Moreover, in these conditions, BayeSlope and, consequently, the adaptive design are also more robust than state-of-the-art methods, such as the GQRS or SWT detectors. However, if we consider the design where BayeSlope is mapped on a PULP-based platform and running on the CL (with the preprocessing modules running on the FC), the device consumes on average 4.6× more than the mapping of REWARD (and the preprocessing) in the FC. In contrast, the adaptive design enhances the energy-accuracy trade-off, maximizing accuracy while limiting energy consumption on modern ULP platforms. This adaptive design is not limited to applications where intense physical exercise is involved, but it can also be applied to pathologies where the ECG morphology changes. Moreover, if BayeSlope is parallelized in the 8-core CL, more computing resources can be assigned to HRV analysis and pathology detection for fully on-node processing to ensure low-rate transmission and data privacy according to the latest remote monitoring healthcare requirements.

VI. Conclusion

In health and wellness monitoring, specifically on the cardiovascular context using wearable systems, there exist multiple pathologies and physical conditions where sudden changes in the measured biosignals occur. In particular, during intense physical exercise, sudden changes in the ECG heart beats amplitude and rhythm cause errors in state-of-the-art standard R peak detection algorithms and, therefore, on any further analysis based on the HR. Moreover, more accurate algorithms often require a higher amount of computing resources leading to a need for more capable wearable platforms with flexible resource management approaches.

In this work, we have proposed a new online machine learning-based design to detect R peaks in a single-lead ECG signal, which adapts at run time to the changes in its morphology. Furthermore, this adaptive design exploits the core heterogeneity of modern ULP wearable platforms, which can run efficiently more complex algorithms using different types of cores. Our new online adaptive design uses a standard lightweight algorithm, REWARD, and an error detection method to measure the algorithm’s accuracy. When REWARD fails, a novel algorithm called BayeSlope, which focuses on robustness to sudden variations in the signal properties though more complex, is triggered and runs in a more capable core. In the context of a maximal exercise test, and, in particular, during high intensity exercise, our proposed BayeSlope outperforms state-of-the-art standard algorithms. Similarly, our online adaptive design achieves a high F1 score, up to 99.0% across five different exercise intensities, which is comparable to always running BayeSlope, and up to 17.5% more accurate compared to running only REWARD.

By implementing the newly proposed adaptive method in the heterogeneous PULP SoC wearable architecture, it can reach energy savings up to 38.7% compared to always running the more complex BayeSlope. Therefore, the newly proposed online adaptive design maximizes the accuracy while minimizing the energy consumption for an optimal energy-accuracy trade-off when used in latest SoC architectures of wearable systems.

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