UNRESOLVED UNIDENTIFIED SOURCE CONTRIBUTION TO THE GAMMA-RAY BACKGROUND

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ABSTRACT

The large majority of EGRET point sources remain without an identified low-energy counterpart, and a large fraction of these sources are most likely extragalactic. Whatever the nature of the extragalactic EGRET unidentified sources, faint unresolved objects of the same class must have a contribution to the diffuse extragalactic gamma-ray background (EGRB). Understanding this component of the EGRB, along with other guaranteed contributions from known sources, is essential if we are to use this emission to constrain exotic high-energy physics. Here, we follow an empirical approach to estimate whether a potential contribution of unidentified sources to the EGRB is likely to be important, and we find that it is. In addition, we show how upcoming GLAST observations of EGRET unidentified sources, as well as of their fainter counterparts, can be combined with GLAST observations of the Galactic and extragalactic diffuse backgrounds to shed light on the nature of the EGRET unidentified sources even without any positional association of such sources with low-energy counterparts.

Subject headings: gamma rays: observations — gamma rays: theory — diffuse radiation

1. INTRODUCTION

The origin of the isotropic diffuse emission (Sreekumar et al. 1998) in energies between 100 MeV and 20 GeV, detected by the Energetic Gamma-Ray Experiment Telescope (EGRET) aboard the Compton Gamma Ray Observatory, remains one of the great unknowns of GeV-energy astrophysics. There are two major questions that still remain unanswered: (1) How much of the diffuse emission detected by EGRET is, in fact, extragalactic, and what is the spectrum of this extragalactic background? (2) What fraction of the extragalactic emission can be attributed to each of the observationally established classes of gamma-ray emitters? Despite the associated uncertainties, these two issues are critical in any attempt to use gamma-ray observations to constrain exotic high-energy physics and yet-undetected classes of theorized gamma-ray emitters.

To answer the first question, a good understanding of the Galactic diffuse emission in the EGRET energy range is required. In order to obtain the intensity and spectrum of the extragalactic emission from the EGRET sky maps, the Galactic emission needs to be modeled and subtracted. This is made complicated by the discrepancy between the observed Milky Way spectrum in energies of \( \gtrsim 1 \text{ GeV} \) and theoretical expectations (Hunter et al. 1997). The observed spectrum is more shallow than model predictions based on the local demodulated cosmic ray spectrum. This deviation is known as the “GeV excess,” and although various explanations have been proposed to account for part or all of the discrepancy, its origin remains a matter of debate (e.g., Pohl et al. 1997; Büsching et al. 2001; Strong et al. 2004b; Kamae et al. 2005; de Boer et al. 2006; Strong 2006; Stecker et al. 2008). As a result, determinations of the gamma-ray background using different Galactic emission models yield very different answers, both in intensity and in spectrum, despite being based on the same set of observations (e.g., Sreekumar et al. 1998; Strong et al. 2004a).

Attempts to answer the second question have been plagued by uncertainties in the cosmic density and evolution of the two established classes of extragalactic gamma-ray emitters: normal galaxies and blazars. Our observational knowledge of the gamma-ray properties of normal galaxies is very limited, as the sample of normal galaxies which have been observed in gamma rays consists of only the Milky Way and a marginal detection of the Large Magellanic Cloud (Sreekumar et al. 1992; Hunter et al. 1997; Hartman et al. 1999). For this reason, the accuracy of theoretical estimates of the contribution of normal galaxies to the gamma-ray background is unavoidably at the order-of-magnitude level (e.g., Lichti et al. 1978; Pavlidou & Fields 2002). But even in the case of blazars, which are by far the most numerous and best-studied class of identified gamma-ray emitters, estimates of their contribution to the gamma-ray background vary from a few percent to 100% of the background originally reported by the EGRET team (e.g., Padovani et al. 1993; Stecker & Salamon 1996a; Kazanas & Perlman 1997; Mukherjee & Chiang 1999; Mücke & Pohl 2000; Narumoto & Totani 2006; Dermer 2007).

The issue is further complicated by the existence of 171 sources which, at the time of publication of the Third EGRET Catalog (hereafter 3EG; Hartman et al. 1999), had not been positively or potentially associated with a lower energy counterpart. These sources are collectively known as the unidentified EGRET sources, and they are more numerous than any established group of gamma-ray emitters. The distribution of these sources on the sky is such that a Galactic feature can be clearly distinguished; however, a large number of sources are located away from the Galactic plane and the Galactic center. No more than a handful of sources can be associated with the Milky Way halo if the Milky Way is not many times brighter in gamma rays than similar galaxies such as M31 (Siegal-Gaskins et al. 2007). Hence, it is almost certain that the EGRET unidentified sources include a significant extragalactic component. Although the nature of these extragalactic sources

\[ \text{Note, however, that the presence of sources at high latitudes does not, in itself, constitute proof that these objects are extragalactic (see, e.g., the Gould Belt discussion in Gehrels et al. 2000).} \]
remains unknown, it is reasonable to believe that there is a large number of fainter, unresolved objects of the same class, which are guaranteed to have some contribution to the extragalactic gamma-ray background (EGRB). If these sources represent yet unidentified members of some known class of gamma-ray emitters (e.g., blazars), then excluding them from any calculation of the contribution of the parent class to the diffuse background would lead to a significantly underestimated result due to an incorrect normalization of the bright end of the gamma-ray luminosity function. If they represent an unknown class of gamma-ray emitters, then the contribution of their unresolved counterparts to the diffuse emission would significantly limit the diffuse flux left to be attributed to known classes, exotic processes, and truly diffuse emission.

Hence, some contribution of unresolved unidentified sources to the EGRB is certain. It is therefore clear that until we either answer the question of the nature of unidentified sources or derive some strong constraint indicating that a possible contribution of such unresolved objects to the EGRB would indeed be minor, we cannot hope to fully understand the origin of the EGRB.

Detailed predictions for the level of the unidentified source contribution to the EGRB involve important uncertainties: since no low-energy counterparts have been identified, we have no estimates of distance, and therefore no estimates of the gamma-ray luminosities of these sources. As a result, very few constraints can be placed on their cosmic distribution and evolution. However, very simple estimates can offer some guidance on whether ignoring this EGRB component may be a safe assumption to make.

For example, we can use the number of unidentified sources, the minimum flux resolvable by EGRET, and the observed intensity to the extragalactic gamma-ray background to place rough limits on the distance scales associated with resolved and unresolved unidentified sources so that unresolved sources do not overproduce the background. A population of unbeamed, nonevolving, single-luminosity sources uniformly distributed in Euclidian space are resolvable out to a distance \( D \) by an instrument of number flux sensitivity \( F_{\text{min}} \). The relation between \( D, F_{\text{min}} \), and number luminosity \( L \) in this case is simply

\[
L = 4\pi D^2 F_{\text{min}}.
\]

If the instrument detects \( N \) such sources, their number density \( n_{\text{src}} \) can be estimated to be

\[
n_{\text{src}} = 3N/4\pi D^3.
\]

If the same distribution of sources continues out to a distance \( d > D \), the isotropic intensity (photons per unit area per unit time per unit solid angle) from the unresolved members of this population will be

\[
I_{\text{unres}} = \int_{d}^{D} dI_{\text{shell}}, \quad \text{where } dI_{\text{shell}} = (1/4\pi)(n_{\text{src}}4\pi r^2 dr)/4\pi r^2
\]

is the contribution from sources within a spherical shell located at a distance \( r \) from the observer. Substituting our results for \( n_{\text{src}} \) and \( L \) above, and performing the integral, we obtain

\[
I_{\text{unres}} = 3NF_{\text{min}}(d - D)/4\pi D.
\]

If we require that the unresolved emission from this population does not exceed the EGRB observed by EGRET \( (I_{\text{unres}} \leq I_{\text{EGRB}}) \), we obtain

\[
I_{\text{EGRB}} \geq 3NF_{\text{min}}(d - D)/4\pi D.
\]

Substituting \( N \sim 100 \) for the population of extragalactic unidentified sources (see discussion in §2), \( F_{\text{min}} \sim 10^{-7} \) photons \( \text{cm}^{-2} \text{s}^{-1} \) for the sensitivity of EGRET, and \( I_{\text{EGRB}} \sim 10^{-5} \) photons \( \text{cm}^{-2} \text{s}^{-1} \text{sr}^{-1} \) (Sreekumar et al. 1998), we obtain \( d \leq 6D \). This result implies that the largest distance out to which such a distribution of objects persists cannot be larger than a few times the distance out to which these objects are currently resolved, since in any other case these sources would overproduce the EGRB. It is therefore conceivable that the unidentified source contribution to the EGRB is significant, if not dominant.

In this work, we approach the problem from a purely empirical point of view. Instead of attempting to predict the level of a diffuse component due to unresolved objects of the same class as unidentified EGRET sources, we try to assess whether there are any empirical indications that this component is, in fact, minor. We construct samples of unidentified sources which, based on their sky distribution, are likely to consist mostly of extragalactic objects. Under the assumption that the majority of these sources can be treated as members of a single class of gamma-ray emitters, we seek to answer the following three questions:

1. Is it likely that unresolved objects of the same class could have a significant contribution to the EGRB at least in some energy range?
2. How would the collective spectrum of their emission compare to the measured spectrum of the EGRB deduced from EGRET observations?
3. How are GLAST observations expected to improve our understanding of the nature of unidentified sources, based on the insight gained from our analysis?

This paper is structured as follows. In § 2 we discuss the samples of resolved unidentified sources used in our analysis. Our formalism for constructing the collective emission spectrum of unresolved unidentified sources is presented in § 3. Inputs from EGRET data used in our analysis are described in § 4. In § 5 we describe our results, and in § 6 we discuss how these results are expected to improve once GLAST observations become available. Finally, we summarize our conclusions in § 7.

2. SOURCE SAMPLES

The observational input constraining our calculations will be the fluxes of the unidentified sources and the spectral index of each source. The fluxes we use for our analysis are the P1234 photon fluxes quoted in 3EG. These fluxes were determined from the combined maps from all viewing periods during which any particular object was within the EGRET field of view. The spectral index \( \alpha \) of each object is also taken from 3EG, and was derived through a fit assuming that the photon flux of each object obeys

\[
F_{\gamma}(E) \propto E^{-\alpha}
\]

where \( E \) is the photon energy.

We seek to constrain a possible contribution to the EGRB from objects of the same class as unidentified sources. For this reason, we would like to base our calculations on a resolved source sample which is as representative as possible of the population of extragalactic unidentified EGRET sources. However, the population of sources which, at the time of publication of 3EG, did not have confident associations with known astrophysical objects, clearly exhibits a Galactic feature, with many of the sources concentrated around the Galactic plane and at small Galactic longitudes (close to the Galactic center). Thus, the original population of EGRET unidentified sources is not an appropriate sample as it includes many sources which are most likely Galactic.

Since these sources are unidentified, there is no counterpart information which could be used to distinguish between Galactic and extragalactic objects. In addition, inferences based on their spectral indices and variability are also very hard to make due to the large error bars associated with measurements of these quantities (see Siegal-Gaskins et al. 2007). Finally, both Galactic and extragalactic unidentified objects exhibit a large range of luminosities, so that inferences about the location of unidentified sources based on their fluxes are not possible either. The only relatively robust indication concerning the location of these sources is their position on the sky. A Galactic population associated with the disk and bulge will most likely be concentrated around low Galactic latitudes and small Galactic longitudes. On the other hand, a halo population, which may appear more uniformly distributed on the sky, cannot have too many members among the resolved EGRET unidentified sources, based on the gamma-ray properties of galaxies similar to the Milky Way (Siegal-Gaskins et al. 2007). Thus,
excluding objects around the Galactic plane and the Galactic center will most likely minimize any Galactic contamination of the sample of unidentified sources.

For this reason, we have excluded from our studies all sources with Galactic latitude $|b| < 10^\circ$ for Galactic longitudes $|l| > 40^\circ$ and Galactic latitude $|b| < 30^\circ$ for Galactic longitudes $|l| \leq 40^\circ$. The source exclusion map we have applied is plotted in Figure 1, and is identical to the mask applied by Sreekumar et al. (1998) in their selection of EGRET diffuse emission data to use for the derivation of the EGRB. The solid angle associated with this mask is $\Omega_{\text{mask}} \approx \pi$, leaving $\approx 3\pi$ of allowed solid angle. For this reason, and under the assumption that an extragalactic population will be uniformly distributed on the sky, we have renormalized all derived flux distributions by a factor of $4/3$.

In addition, we have excluded from all samples objects J0516+2320, J0852−1216, J1424+3734, and J2241−6736 because no P1234 flux was quoted for them in 3EG, and objects J0824−4610, J0827−4247, J0828−4954, J0841−4356, J0848−4429, and J0859−4257 because they were marked as possible or likely artifacts in 3EG.

We have applied further selection criteria which result in three distinct samples of resolved unidentified sources. The use of different samples will allow us to test the sensitivity of our results to the details of the included members:

Sample 1.—All sources which were unidentified at the time 3EG was published and all sources which were characterized as “possible blazars” (identification code “a” in 3EG). These latter objects are routinely not included in studies of the blazar luminosity function, so it is reasonable to examine the potential contribution of this class to the EGRB by including it in our analysis. Sample 1 includes 84 sources.

Sample 2.—Sources which were unidentified at the time 3EG was published. In this case, we do not consider “possible blazars” to belong to this sample. Sample 2 includes 63 sources, and is a subset of sample 1.

Sample 3.—The most conservative of our samples, in that it contains the smallest number of objects. In this case, not only have we excluded all “probable blazars,” but also any object for which even a tentative or potential identification has been suggested since the publication of 3EG. Sample 3 includes 53 sources, and is a subset of sample 2. Sources which are present in sample 2 but not in sample 3 are the following: J0010+7309, J0724−4713, J1212+2304, J1825+2854, J1835+5918, J0329+2149, J0725−5140, J1249−8330, J1621+8203, and J1959+6342.

The locations of all the sources in our samples are shown in Figure 1.

3. FORMALISM

A quantity which, under the assumption of isotropy, fully describes the EGRB is the differential photon intensity $I_E$ (photons per unit area per unit time per unit solid angle). In this section, we calculate $I_E$ for a population of unresolved sources. We make the following assumptions for the population of unresolved gamma-ray sources we consider.

1. Each of the sources has an energy spectrum which, in the EGRET and GLAST energy ranges, can be well described as a single power law of spectral index $\alpha$, and a total photon flux $F_8$ at energies $E > 100$ MeV (where $F_8$ is the photon flux in units of $10^{-8}$ photons cm$^{-2}$ s$^{-1}$).

2. The cumulative flux distribution, $N(>F_8)$ (number of sources with flux greater than $F_8$ vs. $F_8$), of this population can be adequately described, between fluxes $F_{8,\text{min}}$ and $F_{8,\text{max}}$, as a power law,

$$N(>F_8) = CF_8^{-\gamma}. \quad (2)$$

3. The probability distribution of spectral indices of the population $p(\alpha)$ is independent of source luminosity and does not evolve with redshift.

The differential flux of each object of this population, $F_{E_\alpha}$, is related to $F_8$ through

$$F_8 = \int_{E_\alpha}^{\infty} F_{E_\alpha} dE = \int_{E_\alpha}^{\infty} dE \left( \frac{E}{E_0} \right)^{-\alpha} = \frac{F_{E_\alpha} E_0}{(\alpha - 1)}, \quad (3)$$

$^7$ Sample compiled and actively maintained by C. Brown and available online at http://gevsky.org. We stress that suggested associations with lower energy counterparts included in this compilation are simply results reported in recent publications; no effort was made to evaluate the significance and validity of these counterparts by a single uniform standard.
provided \( \alpha > 1 \). Each unresolved source with a flux \( F_8 \) at energies \( > E_0 \) has a contribution \( I_{E,1}(F_8, \alpha) \) to the diffuse emission which is given by

\[
I_{E,1}(F_8, \alpha) = \frac{F_E}{4\pi} = \frac{F_{E_0}}{4\pi} \left( \frac{E}{E_0} \right)^{-\alpha} = \frac{(\alpha - 1)F_8}{4\pi(E_0 \text{ GeV}^{-1})} \left( \frac{E}{E_0} \right)^{-\alpha} \text{ s}^{-1} \text{ sr}^{-1} \text{ GeV}^{-1},
\]

where \( \alpha \) is the spectral index of the source, and \( E_0 = 100 \text{ MeV} \) in the case of 3EG fluxes. The \( 1/4\pi \) normalization factor comes from assuming an isotropic distribution of sources, the collective emission of which is uniformly distributed over the celestial sphere.

The differential flux distribution of the population is

\[
\frac{dN}{dF_8} = \kappa F_8^{-\alpha - 1}. \tag{5}
\]

The collective diffuse emission due to this population of unresolved sources with fluxes between \( F_{8,\text{min}} \) and \( F_{8,\text{max}} \) will be

\[
I_E(E) = \int_{F_{8,\text{min}}}^{F_{8,\text{max}}} dF_8 \int_{-\infty}^{\infty} d\alpha \frac{dN}{dF_8} p(\alpha) I_{E,1}(F_8, \alpha),
\]

\[
= I_0 \left[ \frac{\kappa F_8^{-\alpha - 1}}{-\kappa + 1} \right] F_{8,\text{max}}^{\alpha - 1} \int_{-\infty}^{\alpha} d\alpha p(\alpha) \left( \frac{E}{E_0} \right)^{-\alpha} (\alpha - 1), \tag{6}
\]

where \( I_0 = 10^{-7} \text{ cm}^{-2} \text{ s}^{-1} \text{ sr}^{-1} \text{ GeV}^{-1}/(4\pi) \). Physically, the upper limit flux \( F_{8,\text{max}} \) represents the sensitivity limit of the telescope (objects with flux higher than this are resolved and do not contribute to the background), while the lower limit flux \( F_{8,\text{min}} \) represents the flux below which the approximation of equation (2) for the cumulative flux distribution breaks down. The features of the spectral shape of this emission in the simple case when \( p(\alpha) \) is a Gaussian are discussed in Appendix C.

4. Inputs from EGRET Data

Equation (6) can provide a first simple estimate for the possible contribution of unresolved sources of the same class as extragalactic unidentified EGRET sources to the isotropic diffuse gamma-ray background. The required inputs are the cumulative flux function of equation (2), and the spectral index distribution of the source class, \( p(\alpha) \). In this section, we derive these inputs from the three source samples discussed in §2. Possible source variability has not been accounted for in this analysis. A discussion of possible effects of source variability, as well as our reasoning for not considering them for the purposes of our study, are presented in Appendix B.

4.1. The Cumulative Flux Distribution

We use data from the resolved objects in our three samples to construct the cumulative flux distribution of EGRET unidentified sources. The cumulative flux distributions of the three samples are shown in Figure 2. Due to nonuniformities in EGRET exposure, the lowest resolvable flux is not a hard-set number, but rather the efficiency in resolving low-flux objects decreases gradually as the flux decreases, which is one of the major factors in the slow turnover of the cumulative distribution function. For this reason, we only use data within the range \( F_{8,\text{max}} < F_8 < F_{8,\text{N=5}} \) to obtain a fit to the cumulative flux distribution. We take \( F_{8,\text{max}} = 6 \) and assume that all sources with fluxes above this limit have been resolved by EGRET. We define \( F_{8,\text{N=5}} = 6 \text{ to be the flux for which, in each sample, five objects with fluxes higher than or equal to it have been resolved. The best-fit values of } C \text{ and } \kappa \text{ for each sample are shown in Table 1. As we can see in Figure 2, as well as from the parameter values in Table 1, the slopes of the cumulative flux distribution in the regime where most objects are expected to have been resolved by EGRET are fully consistent with each other. This in turn implies that the data are consistent with the hypothesis that most members of all samples have been drawn from a single population of extragalactic emitters.}

However, we note that the flux distribution slope, close to \( \sim 2.5 \) in all cases, is steeper than the slope that would be expected from a single-luminosity population of sources with a uniform distribution in a flat cosmology (which is equal to 1.5; e.g., Dermer 2007) and is also steeper than the slope of the flux distribution of the confidently identified blazar population. This result may reflect the cosmological distribution and evolution properties of the population of extragalactic unidentified sources. However, it may also originate in a selection effect in the identification of gamma-ray sources: the positional identification of brighter sources is more frequent as more photons are detected from these sources which allows for a more
accurate pinpointing of their location. In addition, multiwavelength campaigns for the identification of gamma-ray sources naturally target the brightest objects first. For these reasons, the high-flux end of the flux distribution may be preferentially depleted, which would lead to an apparent steepening of the distribution of the sources that remain unidentified. Finally, the steepness of the slope could be an effect of viewing a distribution with real curvature in a very small dynamical range in flux. A simple example quantifying such a possible effect is the following: if we were to treat all sources in sample 1 and all confidently identified blazars which are located outside our exclusion mask as a single population, then the cumulative flux distribution power-law fit in the flux range \(6 < F_8 < F_{8,N=5}\) would have a slope \(\kappa = 1.63 \pm 0.03\), much closer to 1.5.

Finally, we should add a cautionary note on fits to the cumulative, rather than differential, flux distribution function, such as the one presented here. Our fits purposefully do not account for uncertainties in each bin since, from a statistical point of view, such uncertainties are almost perfectly correlated (each bin contains the same data as its adjacent ones plus/minus one data point). On the other hand, the poor dynamical range in flux and the dependence of uncertainties of the differential flux function on the size of the bin make constructing and fitting the differential flux function problematic as well. For these reasons, it is important to not over-interpret these results, which should be viewed as broad, order-of-magnitude assessments of the behavior of the flux distribution, rather than robust statistical evaluations and strict constraints.

### 4.2. The Spectral Index Distribution

The second important observational input in our calculation is the distribution of spectral indices of unidentified objects \(p(\alpha)\). In the limit that the spectral index of sources is independent of source redshift and luminosity, the spectral index distribution uniquely determines the spectral shape of the collective emission from the unresolved population. The spectral shape of the unresolved emission provides, in turn, an additional tool to assess the possibility that unidentified sources constitute a dominant contribution to the EGRB through shape comparison between the observed and the predicted spectra of diffuse extragalactic emission.

In our analysis we adopt the assumption that the spectral index distribution of unresolved unidentified sources is the same as that of the resolved unidentified sources. The latter can be deduced from measurements of the spectral index \(\alpha\) for sources in each one of our samples, following the method presented in Venters & Pavlidou (2007). The details of this calculation, properly accounting for measurement uncertainties in individual spectral indices of resolved sources, are presented in Appendix A.

### 5. RESULTS

As is immediately obvious from equation (6), the shape and the overall normalization \(I_0\) of the cumulative emission from unresolved unidentified sources are decoupled under our assumptions. The shape of the spectrum depends on the spectral index distribution, while the normalization, given a fit to the flux distribution, depends only on \(F_{8,\text{min}}\) (the value of the flux where the extrapolated power law breaks).

Assuming that, close to the EGRET flux limit, the flux distribution does not evolve drastically, an extrapolation of the measured flux function to lower fluxes can be considered representative of its behavior in the low-flux regime. This assumption is less likely to hold as the limiting flux to which we are extrapolating becomes lower: the flux distribution will eventually exhibit a break due to cosmological effects and/or luminosity evolution. The question is how far in the low-flux regime our extrapolation must continue before we get a significant contribution of unresolved unidentified sources to the gamma-ray background. If the answer is “not very far,” then our extrapolation may indeed be reasonable over such a small range, and unresolved, unidentified sources are likely make up a considerable fraction of the EGRB. On the other hand, if we need to extrapolate the flux distribution down to fluxes very low compared to the resolved flux range, then it is quite unlikely that our extrapolation is valid throughout the flux regime in which we use it. In such a case it is doubtful that the actual flux distribution of the unresolved unidentified sources is such that unidentified sources make up a significant portion of the EGRB.

We use observations of the EGRB to determine by what value of \(F_{8,\text{min}}\) the extrapolated flux distribution power law must break, so that the background is not overpredicted at any energy range. To ensure that we are placing the most conservative constraint (i.e., that we allow extrapolation to the lowest fluxes possible), we will use the most generous observational determination of the EGRB, which is that of Sreekumar et al. (1998). The requirement that this background is not exceeded for any energy above 100 MeV returns the limiting breaking fluxes indicated by the three vertical lines in Figure 2. Our results then indicate that, for any of our three samples, we would only need to extrapolate the cumulative flux distribution for at most an order of magnitude below the lower limit of the resolved flux range to have unresolved unidentified sources comprise most of the EGRB, at least at low energies. This is not an extreme extrapolation, and therefore a significant contribution by the “unidentified” class to the diffuse background is likely.

In order to interpret this result correctly, we should assess the qualitative and quantitative uncertainties associated with it. First of all, a power-law extrapolation of the flux distribution to lower, unresolved flux values even for only 1 order of magnitude in flux is by no means self-evident, although it is the simplest and most straightforward assumption. For example, the Dermer (2007) fits to the flux distribution of resolved blazars (using a model based on the cosmological evolution of black hole jet sources) increase less steeply than a power law even very close to the EGRET sensitivity limit. It is conceivable that unresolved members of the extragalactic unidentified source class could have a comparable cosmic evolution, and a similar behavior in the flux function. In fact, our tight constraints on the power-law extrapolation of the flux function may be taken to imply just that: the cosmological evolution of these sources has to be such that the flux function deviates from a power-law form very fast, to ensure than unresolved members of this class do not overproduce the EGRB.

Second, statistical and systematic uncertainties in the power-law fits to the cumulative flux function have to be taken into account. In our case, the systematic uncertainties associated with the sample selection and the small dynamical range in flux over which the flux function is sampled dominate over the statistical uncertainties in the power-law slope derived in the selected flux range, shown in Table 1. The most extreme case is the one where unidentified sources are considered as a unified sample with identified blazars outside the mask. In this case, as discussed in § 4.1, the flux function slope is considerably shallower, allowing for a more extended extrapolation to low fluxes before the EGRB is overproduced. The lowest flux limit allowed for the extrapolation in this case is shown with the gray line in Figure 2, and is a moderate factor \(~3\) below the limits of the unidentified source samples when considered alone.

A comparison between the shape of the cumulative emission spectrum of unresolved unidentified sources and the EGRET EGRB
The unresolved emission from unidentified sources, entering through their model of the Galactic component from the EGRET diffuse sky map. The dotted lines are the systematic uncertainties in the EGRB determination of Strong et al. (2004a), entering through their model of the Galactic component from the EGRET diffuse sky map. The dotted line shows a single power-law fit to the spectrum of the unresolved unidentified source emission for sample 1, entering through the statistical uncertainty in the ISID parameters.

is shown in Figure 3. The dashed line shows a single power-law fit to the Sreekumar et al. (1998) determination of the EGRB. The thick solid line is the more recent redetermination of the gamma-ray background by Strong et al. (2004a), in which they used a more detailed model of the Milky Way diffuse emission to subtract the Galactic component from the EGRET diffuse sky map. The dotted lines are the systematic uncertainties in the EGRB determination of Strong et al. (2004a), entering through their model of the Galaxy. Our calculation of the spectrum of the unresolved unidentified source component is shown with the thick solid line. The maximum likelihood parameters from sample 1 were used for $p(\alpha)$ in this calculation, although, as becomes clear from Figure 5 in Appendix A, the spectral shapes resulting from all three samples are consistent with each other. At low energies, where the systematics are low, the spectrum of the unidentified component is in excellent agreement with the EGRB observational spectrum of Strong et al. (2004a). At higher energies, where the systematics are large, the unidentified component spectrum is largely within systematics except at very high energies. If unidentified sources are indeed a dominant contribution at relatively low energies, then this result may be perceived as a tantalizing hint that at the highest energies of the EGRET range a new type of contribution, (e.g., from high-energy peaked BL Lacs, or from annihilating dark matter) may become important at $\sim 1$ GeV.

It should be noted that the amplitude of the cumulative spectrum plotted in Figure 3 does not constitute a prediction; rather, it is the maximum possible emission allowed from unresolved unidentified sources so that the observed EGRB is not exceeded in any energy bin above 100 MeV. In Figure 3 we also overplot, with the thick gray lines, the 1 $\sigma$ uncertainty in the spectral shape of the unresolved emission from unidentified sources, entering through uncertainties in the intrinsic spectral index distribution (ISID) parameters.

6. PROSPECTS FOR GLAST

The launch of GLAST in 2008 will provide significant new insight into the nature of unidentified sources and their possible contribution to the EGRB. The ideal solution to the unidentified source puzzle would be, of course, the direct positional association of all unidentified sources with undisputed low-energy counterparts. This would then allow us to build more confident models for the unresolved members of these classes of objects. However, such an outcome is unlikely, as the large number of possible counterparts and the large number of sources which we expect GLAST will be able to resolve make multiwavelength campaigns for every single source impractical.

However, there is another definitive test that GLAST will be able to perform which does not require confident identification of each source to provide information about the likely nature of unidentified sources as a population. With the increased flux sensitivity of GLAST, many more objects of the same class will be resolved. If these objects are mostly extragalactic, as assumed here, and if they comprise a significant fraction of the EGRET EGRB, as suggested by our analysis, then there will be an associated decrease of the EGRB from its EGRET levels, equal to the all-sky–averaged intensity of the newly resolved objects. The flux sensitivity of GLAST is expected to be about 50 times better than that of EGRET.\(^8\) Therefore, GLAST will be able to probe the flux distribution of unidentified sources down to fluxes close to $F_{\text{min}}$ and definitively test our empirical estimate.

If, on the other hand, even high-latitude unidentified sources are mostly Galactic (which would imply that the Milky Way may be unusually bright in gamma rays), then there will be an associated reduction of the Milky Way diffuse emission rather than of the isotropic background (for a discussion on a possible contribution of a large number of Galactic point sources to the Galactic diffuse emission and the role of such sources in explaining at least in part the origin of the GeV excess, see Strong 2006).

GLAST will not only represent a leap in instrument sensitivity, but also in energy range, as it will allow access to the yet-unexplored range between a few tens and a few hundreds of GeV. Sources with fluxes high enough that measurements of their spectra can be extended in this range will have an additional indicator of their location (Galactic vs. extragalactic): if they are located at cosmic distances, a feature generated by attenuation of gamma rays on the extragalactic background light may be detectable; on the other hand, if they are located within the Milky Way, no such feature should be present.

In addition, GLAST observations will improve the inputs used in our calculation. Spectral indices, at least for the brighter sources, will be measured with much greater accuracy. This will improve our constraints on $p(\alpha)$ and the shape of the cumulative emission from unidentified sources. In addition, spectral discrimination between different classes of unidentified emitters may become possible. Finally, the dynamical range over which fluxes will be measured will increase significantly, and any biases in the calculation of the slope of the flux distribution of high-latitude unidentified sources will become less pronounced.

7. DISCUSSION AND CONCLUSIONS

In this work, we have used a purely empirical model to explore the possibility that unresolved gamma-ray sources of the same

\(^8\) See http://www-glast.stanford.edu/mission.html.
class as unidentified EGRET sources have an appreciable contribution to the EGRB. We have argued that some unidentified source contribution to the gamma-ray background is guaranteed. We have additionally found that (1) if most high-latitude unidentified sources are assumed to be extragalactic, a one order of magnitude extension of the cumulative flux distribution to lower energies without breaks implies a significant contribution to the EGRB, at least at the lower part of the EGRET energy range; and (2) the spectrum of the cumulative emission of such unresolved sources would be very consistent with the observational determination of Strong et al. (2004a) of the EGRET EGRB within systematics.

We emphasize that the purpose of this study is not to estimate, even at the order-of-magnitude level, the diffuse flux expected from extragalactic unresolved unidentified sources, but rather to place constraints on the flux distribution of these objects under the constraint that the measured background should not be exceeded in any energy interval. Our treatment is therefore different in purpose and spirit from most past work aiming to estimate the level of the contribution of different populations to the extragalactic gamma-ray background. Such work has been traditionally of two types. The first involves population models built from some understanding of the physics of the sources (such as, e.g., the models of Mücke & Pohl [2000] and Dermer [2007] in the case of blazars; Miniati [2003], Keshet et al. [2003], Blasi et al. [2007] in the case of clusters of galaxies; and Lichte et al. [1978] and Pavlidou & Fields [2002] in the case of normal galaxies). The second involves models of the population luminosity function based on our knowledge of the source population from other wavelengths and normalized to fit EGRET data (such studies require a sample of detected, identified members, and are therefore applicable to blazars only; e.g., Chiang et al. 1995; Stecker & Salamon 1996b; Mukherjee & Chiang 1999; Narumoto & Totani 2006). In our case, lacking any knowledge of the physics of sources as well as of even the bright end of the luminosity function (since in absence of identifications no redshift and hence no luminosity can be derived for any of the sources), we have reversed the problem. Instead of using some assumed cosmic evolution for the sources to derive the expected level of contribution to the EGRB, as in all of the investigations mentioned above, we have used the tightest possible constraint on the allowable EGRB contribution of these sources (the observed EGRET background) to constrain the flux distribution of the unresolved sources. Our conclusions for the overall expected unresolved unidentified source intensity come from the observation that our constraints on the flux distribution are indeed very tight; hence, the contribution of the unidentified sources to the EGRB is likely to be high.

Our analysis suggests that any model of the EGRB would be incomplete without some treatment of the unidentified source contribution. The results of our empirical model therefore motivate the pursuit of specific population models for the unidentified sources. Although such models involve a more restrictive set of assumptions and increased uncertainties, they can provide more concrete predictions for the luminosity function of unresolved objects. Once a luminosity function model is assumed, and under the assumption that unresolved members of this class do indeed contribute most of the extragalactic diffuse emission, additional estimates can be made regarding the distance scales associated with this population. The dynamical range in fluxes of the resolved members of the population, as can be seen in Figure 2, is smaller than an order of magnitude. For a single-luminosity population, this corresponds to a factor of 3 dynamical range in distance, which increases or decreases if the typical source luminosity increases or decreases with increasing redshift, respectively. Such arguments can constrain not only the distance scales, but also the number density, intrinsic brightness, and evolution of the resolved and unresolved objects, if in a model-dependent fashion. Additional constraints and predictions, once a luminosity function has been assumed, can be derived through the multimessenger and multiwavelength approach. If the emission from extragalactic unidentified sources is primarily of hadronic origin, it will be accompanied by neutrinos at comparable fluxes, and that may have potentially observable consequences in the TeV range for future km$^3$ neutrino detectors such as IceCube and Km3Net. If on the other hand the gamma-ray emission is primarily leptonic, it will be accompanied by X-ray emission, and their extragalactic background flux in the X-ray band may provide an additional constraint. We will pursue such models and calculations in an upcoming publication.

In this work we have tried, where possible, to make assumptions, which, if anything, underestimate the possible contribution of unresolved unidentified sources to the EGRB. An exception to this general trend is our working assumption that the majority of the resolved, high-latitude 3EG unidentified sources belong to a single class. It is conceivable that instead, the resolved unidentified sources are a collection of members of several known and unknown classes of gamma-ray emitters. In this case, it is still likely that the summed contribution of unresolved members of all parent classes to the diffuse background is significant. However, the construction of a single cumulative flux distribution from all sources and its extrapolation to lower fluxes is no longer an indicative test for the importance of such a contribution.

Although we have argued that the contribution of unresolved unidentified sources to the EGRB is likely to be important or even dominant, the cumulative emission spectrum derived here and presented in Figure 3 is only an upper limit, as it was derived demanding that the observed EGRB is not exceeded at any energy above 100 MeV. The contribution of unresolved unidentified sources is further constrained by allowing for the presence of the guaranteed contributions of unresolved normal galaxies and blazars.

Finally, it is noteworthy that we have found no evidence for an inconsistency between the population properties of high-latitude unidentified sources and those of blazars. The presence of a yet-unknown population of extragalactic high-energy emitters among the high-latitude EGRET unidentified sources remains one of the most tantalizing possibilities in GeV astronomy and one of the most exciting prospects for the GLAST era. However, the presently available data on the spectral index distribution and the cumulative flux distribution of these sources (this work), as well as their variability properties (e.g., Nolan et al. 2003), are consistent with their being members of the blazar population. If indeed a large number of members of the blazar class are present among the extragalactic unidentified sources, then this could have potentially serious effects on our understanding of the redshift distribution of resolved blazars and consequently of the blazar luminosity function.

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APPENDIX A

ESTIMATING THE SPECTRAL INDEX DISTRIBUTION OF EXTRAGALACTIC UNIDENTIFIED SOURCES

Figure 4 shows a histogram of the spectral indices of the sources in sample 1 (solid line). The typical measurement uncertainty for any single spectral index (thick solid line) is comparable with the spread of the distribution, so the spread of a simple binning of spectral indices might not in fact give us information about the underlying distribution of the spectral indices of the sources, but rather be representative of the uncertainty of each single measurement.

Following an analysis similar to that of Venters & Pavlidou (2007) for the case of blazars, we assume that the intrinsic spectral index distribution (ISID) of unidentified sources can be approximated by a Gaussian,

\[
p(\alpha) = \frac{1}{\sqrt{2\pi}\sigma_0} \exp\left[-\frac{(\alpha - \alpha_0)^2}{2\sigma_0^2}\right].
\]

(A1)

Lacking any knowledge to the contrary, this choice not only simplifies the subsequent statistical analysis, but also renders the spectral shape part of equation (6) analytically integrable (see Appendix C). We then use a maximum likelihood analysis which takes into account the individual errors of measurement of \(\alpha\) for each source by introducing the true spectral indices of the sources as nuisance parameters and by marginalizing over them. The likelihood in this case, omitting constant normalization factors, is (Venters & Pavlidou 2007)

\[
\mathcal{L} = \left(\prod_{j=1}^{N} \frac{1}{\sqrt{\sigma_0^2 + \sigma_j^2}}\right) \exp\left[-\frac{1}{2} \sum_{j=1}^{N} \frac{(\alpha_j - \alpha_0)^2}{\sigma_0^2 + \sigma_j^2}\right],
\]

(A2)

where \(\alpha_j\) and \(\sigma_j\) are the measured spectral index and the associated uncertainty of this measurement for a single source. Table 2 shows the maximum likelihood \(\alpha_0\) and \(\sigma_0\) for each sample. The maximum likelihood spectral index distribution for sample 1 is plotted with the dashed line in Figure 4, and indeed is narrower than the histogram.

Figure 5 shows 1, 2, and 3 \(\sigma\) contours for the likelihood of equation (A2), as calculated using sample 1 data (solid line). The location of the maximum is indicated by cross signs, while the corresponding maxima of the sample 2, and sample 3 likelihoods are indicated by a square and a triangle, respectively. In both cases, the location of the maximum is within the 1 \(\sigma\) contour of sample 1. As an

| Parameter | Sample 1 | Sample 2 | Sample 3 |
|-----------|----------|----------|----------|
| \(\alpha_0\) | 2.38     | 2.39     | 2.40     |
| \(\sigma_0\) | 0.22     | 0.24     | 0.19     |
additional comparison, we overplot, with dashed lines, the 1, 2, and 3 \( \sigma \) likelihood contours for the sample of the 46 confidently identified blazars of Mattox et al. (2001). The figure demonstrates that extragalactic unidentified sources are spectrally consistent, at the 1 \( \sigma \) level, with being blazars.

APPENDIX B
SOURCE VARIABILITY

Certain classes of sources contributing to the gamma-ray background may exhibit significant time variability (blazars are a prominent example of such sources). This fact has generated some concern that the objects resolved by EGRET (especially the fainter ones) are preferentially objects that happened to be in their flaring state when observed, and hence the luminosity function as determined by the resolved objects is not an adequate description of all the unresolved sources contributing to the gamma-ray background. Stecker & Salamon (1996a) have addressed that uncertainty in the case of blazars using an explicit treatment of source variability.

This concern is less pronounced if the fluxes used for normalizing the luminosity function of a class of sources are averaged over exposure times reasonably large compared to the source duty cycle. To minimize the possible impact of variability, we use in this study the P1234 fluxes quoted in 3EG. Sources which have been detected in individual viewing periods but which have no P1234 flux (which implies that their detection significance in the cumulative map was not high enough) are omitted from our analysis.

We have not made any further attempt to treat variability in this work, because the unknown parameters in the variability properties of sources are severe enough that any simple treatment of variability is likely to introduce at least as much uncertainty as it attempts to remove, while any uncertainty in the flux distribution of the source samples due to source variability is minor compared to the uncertainties introduced due to our ignorance concerning the nature of unidentified sources. We have simply used the time-averaged flux of resolved unidentified sources as representative of the emission properties of such sources.

APPENDIX C
SPECTRAL SHAPE OF CUMULATIVE UNRESOLVED POINT-SOURCE EMISSION

The spectral shape of the cumulative emission from a population of unresolved sources with individual power-law photon spectra \( F_\nu \propto \nu^{-\alpha} \) and a Gaussian spectra index distribution \( p(\alpha) \) is given by equation (6). If \( p(\alpha) \) is a Gaussian of the form of equation (A1), as assumed here, then equation (6) can be integrated analytically. Defining \( I_0 = I_0[(\kappa CF_8^{-\kappa+1})/(1-\kappa)]_{E_{\text{min}}}^{E_{\text{max}}} \), we can write

\[
I_\nu(E) = \tilde{I}_0 \int_{\infty}^{E} d\alpha (\alpha - 1) \frac{1}{\sqrt{2\pi}\sigma_0} \exp \left( -\frac{(\alpha - \alpha_0)^2}{2\sigma_0^2} \right) \exp \left( -\alpha \ln \frac{E}{\overline{E}_0} \right)
\]

\[
= \frac{I_0}{\sqrt{2\pi}\sigma_0} \exp \left( -\frac{B_0}{2\sigma_0^2} \right) \int_{\infty}^{E} d\alpha (\alpha - 1) \exp \left( -\frac{(\alpha - A_0)^2}{2\sigma_0^2} \right) = \tilde{I}_0(A_0 - 1) \exp \left( -\frac{B_0}{2\sigma_0^2} \right).
\]

(C1)
where $A_0 = \alpha_0 - \sigma_0^2 \ln(E/E_0)$ and $B_0 = 2\alpha_0 \sigma_0^3 \ln(E/E_0) - \sigma_0^4 \ln(E/E_0)^2$. The usual way of plotting the isotropic background spectrum is $E^2 I_E$ versus $E$ in logarithmic scale (as in Fig. 3). Defining $X = \ln(E/E_0)$ and $Y = \ln(E^2 I_E)$, we can rewrite equation (C1) as

$$Y = \frac{\sigma_0^2}{2} X^2 - (\alpha_0 - 2)X + C + \ln(\alpha_0 - 1 - \sigma_0^2 X)$$

where $C = \ln(\tilde{I}_0 E_0^2)$. Note that the limits of integration of equation (C1) should strictly extend from $\alpha = 1$ (instead of $-\infty$) to $\infty$, to ensure that all $F(> 100$ MeV) are positive and finite. The result of equation (C1) is a good approximation as long as $\alpha_0$ is high enough and $\sigma_0$ is low enough so that $p(\alpha)$ has no appreciable power at $\alpha < 1$. Equation (C2) consists of a parabolic convex part and a logarithmic concave part. The parabolic part dominates at low energies and is responsible for the characteristic convex shape of the unresolved emission from a population of sources with power-law spectra and a finite-spread spectral index distribution (see, e.g., Brecher & Burbidge 1972; Stecker & Salamon 1996a, 1996b; Pohl et al. 1997). The spectrum remains convex ($d^2 Y/dX^2$ is positive) for $X < (\alpha_0 - 1)/\sigma_0^2 - 1$. The curvature of the spectrum depends on the spread of the spectral index distribution, $\sigma_0$ (the second-order term coefficient in eq. [C2] is $\sigma_0^2/2$). Consequently, an overestimation of the spread of the population spectral index distribution will lead to an overestimation of the curvature of the corresponding unresolved emission spectrum (as pointed out by Pohl et al. [1997], Pavlidou et al. [2007], and Venters & Pavlidou [2007]). In the limit $\sigma_0 \to 0$ all sources have identical spectra of index $\alpha_0$, and equation (C2) yields a power law, $Y = \text{constant} + (\alpha_0 - 2) X$ or, equivalently, $I_E \propto E^{-\alpha_0}$, as expected. For $\sigma < 0.5$, equation (C2) has a local minimum, at $X = [2\alpha_0 - 3 - (1 - 4\sigma_0^2)^{1/2}] / (2\sigma_0^2)$, which corresponds to the energy at which the population has the smallest energy flux contribution to the (unabsorbed) isotropic background.

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