The Influences of NP100 Surfactant and Pine-Oil Concentrations on Filtrate Volume and Filter-Cake Thickness of Microemulsion-Based Drilling Fluids (O/W)

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Abstract: In this work, nonionic surfactant NP100 and pine oil influences on the filtrate volume (FV) and the filter-cake thickness (thkns) of microemulsified drilling fluids were studied. A ternary phase diagram was obtained to define the microemulsion region, where a 2⁴ factorial design was used with the addition of four center points and axial points. Twelve microemulsion points were defined and used later in the formulation of the investigated drilling fluids. The results showed that the increase in the surfactant and pine oil’s concentration increased FV and thkns, with the oil phase being the most influential component in the filtrate volume and the surfactant being the most influential in the filter-cake thickness. Statistically significant models were obtained. The optimal concentrations were determined for the lowest FV and thkns; 45% of surfactant and 5% of pine oil for the filtrate volume (1.3 mL), and 45% of surfactant and 15% of pine oil for the filter-cake thickness (0.64 mm).

Keywords: microemulsion; drilling fluid; filtrate volume; filter-cake thickness; experimental design

1. Introduction

Oil and natural-gas productions involve drilling wells into the reservoir, and the success of this operation depends, among other factors, on the efficiency of the drilling fluid used. The drilling process is carried out using a drill bit connected to a long drill pipe sequence [1–5]. Applying a downward force and rotation to the drill bit, it crushes the rock into small cuttings, and with the action of the drilling fluid that circulates from the surface through the drill pipe onto the drill bit’s face, these cuttings are brought up to the surface [1,6,7].

In addition to removing these cuttings, drilling fluids perform essential functions such as cooling and lubricating the drill bit, stabilizing formation pressures, and allowing an adequate geological-formation evaluation. Regarding the wellbore walls, the drilling fluids reduce the friction between the drill pipe and the wellbore walls and form a low-permeability film (filter cake) to prevent or mitigate the invasion of the filtrate into the rock formation [8,9]. According to Civan [9], mud fines and filtrates are prone to invade and damage the near-wellbore formations. The drilling fluid should also prevent or minimize the swelling of hydratable clays from the formation. These functions make drilling fluids indispensable to the oil industry [10–13].

Two of the main problems and challenges related to drilling activity are the fluid loss and gradual increase in the filter cake that can cause damages to the wells and increase the drilling cost. Generally, these two problems coincide in the drilling activity. The fluid loss will cause severe damage to the formation and the particle size distribution on the lost material, the latter being one of the essential factors in fluid-loss control and protecting the
Hence, a suitable drilling practice involves controlling the drilling-fluid filtration, whereas an inadequate design may be associated with borehole instability, excessive torque and drag, pressure-differential sticking, and, as mentioned before, formation damage [16]. The control of drilling-fluid filtration characteristics includes managing the filtrate volume per unit area and unit time and the quality of the resulting filter cake formed in the wellbore [17].

The filter cake's formation on the wellbore walls is an essential parameter in fluid loss, so the drilling fluid should form a thin, impermeable filter layer that presents excellent sealing properties. Simultaneously, this filter cake is expected to minimize fluid permeation and drilling solids in the formation and withstand a high unbalanced differential pressure [11,18]. Microemulsion-based drilling fluids directly contribute to an efficient formation of this filter cake, as there is a significant reduction in the tensions between the drilling fluid and the wellbore surface, so the fluid loss is minimized [19–21].

Microemulsions were first observed by Schulman [22] and Winsor [23] and were extensively researched between the 1970s and 1980s, motivated by two oil crises in 1973 and 1979, respectively [24]. These structures are macroscopically isotropic mixtures composed of at least one hydrophilic, one hydrophobic, and one amphiphilic component, and they are both thermodynamically stable and transparent [25,26]. Thus, they can be defined as high-aggregation systems in which water and oil are homogeneously mixed due to amphiphilic substances called surfactants [27]. In general, microemulsions are an excellent option to replace non-aqueous drilling fluids, as they present considerable thermal stability, reduced costs, and exemplary performance in different types of formation. Another critical advantage presented by microemulsions is their environmentally friendly status, as they are based on non-damaging components.

The use of surfactants in water-based drilling fluids is already known in the literature. For instance, nonionic surfactants such as Tween 80/ZnO nanoparticles [28] and 2-hexadecyloxyethanol [29] have been applied in water-based drilling fluids to enhance their rheological properties, lubricity, and clay-inhibition behavior. The nonionic surfactant Tween 80 increases the drilling fluid's viscosity and provides clay-swelling inhibition and coating characteristics, improving rheology, filtrate loss, lubricious property, and clay-inhibition behavior of water-based drilling fluids.

Drilling fluid properties may be modified by the use of nanocomposite additives, such as TiO$_2$/Polyacrylamide (PAM), through the polymerization of acrylamide monomer in the presence of high-hydrophilic–lipophilic-balance (HLB) surfactants, such as sodium dodecyl sulfate and Tween 80, obtaining lower filter-cake thickness and fluid loss as it increases the surfactant concentration [30]. The performance of drilling fluids may also be affected by the formulation of the kind of surfactant (nonionic or ionic) [31], especially a nonionic surfactant, which presents a higher HLB, as it provides low filtrate loss and filter-cake thickness. The same sort of performance was achieved when the nonionic surfactant Span 80 [32] and other additives were used to synthesize core-shell nanocomposites to replace the traditionally applied CaCO$_3$ as a bridging agent, resulting in higher performance in filter-cake thickness and fluid-loss control.

Alongside the various other applications of nanomaterials, such as enhanced oil recovery, wettability alteration, and interfacial-tension reduction (IFT) between reservoir fluids, they are being used in work to improve rheological properties, filtration loss, and viscosity, among other things [33–35]. TiO$_2$ nanoparticles-bentonite (TNBT) nanocomposites are also used to improve the properties of drilling fluids, especially concerning fluid loss and filter cake. They act directly to improve the fluid’s lubricity (0.24 to 0.28) [36], as do microemulsions, which also provide good lubricity coefficients in drilling fluids (0.12 to 0.20) [35], lower filter-cake thickness, and stabilization of the wellbore [35,37]. They also may improve clay- and shale-swelling inhibition for water-based fluids. The clay swelling may cause an increase in viscosity due to the expansion of bentonite in water, which increases the drilling fluid’s viscosity. Therefore, microemulsions can reduce water intake in the pores.
The nonionic surfactant Ultranex NP100, used in this work, presents excellent emulsifying properties, like TW80. NP100 has a hydrophilic head that can attract toward a clay surface, thus coating it, and a hydrophobic tail that can repel water molecules, which are both of the most frequent characteristics of potential shale inhibitors [38]. However, NP100 has been used not as an additive for water-based drilling fluid (WBDF) but as the continuous phase per se, with an aqueous phase composed of water-glycerol and low-cost vegetable oil as an oil phase. Microemulsion-based drilling fluids are considered low-cost, environmentally friendly, and present excellent thermal properties, providing low filtrate volume and filter-cake thickness.

Microemulsion-based drilling fluids present certain advantages over conventional drilling fluids. They have been used due to their reduced costs, stabilization when facing various formation types, and reduced environmental damage [39–42]. Considering the microemulsion-based drilling fluids formed by a nonionic surfactant, an aqueous phase, an oil phase, and additives, this work aims to study the influences of the NP100 surfactant (nonionic and biodegradable) and pine oil (vegetable oil) on the formation of the filter cake and filtrate volume, in order to obtain environmentally acceptable drilling fluids.

2. Materials and Methods

An experimental flowchart and step-by-step procedures for conducting the laboratory work of the present study are illustrated in Figure 1. The work can be divided as such: (i) A brief description of the ternary phase diagram along with the components that make up the microemulsion (nonionic surfactant NP100, pine oil, and water-glycerol solution) to determine the area of interest. This step is of fundamental importance to prepare the drilling fluids. Experimental planning was adopted to investigate the desirable region, and the 12 drilling fluids design (4 in factorial points, 4 in axial points, and 4 in central points) was determined. However, the experimental design is presented in detail only in the results. (ii) An introduction to the basic methodology for examining the drilling fluids and all the tests in which the formulated fluids were submitted: rheology, filtrate volume, and filter-cake thickness and permeability. (iii) The results for all fluids formulated within the experimental design. (iv) A statistical analysis based on the obtained results.

![Figure 1. Experimental flowchart of the steps used in this study.](image)

2.1. Ternary Phase Diagram

The ternary phase diagram (Figure 2) was created by plotting the mass fractions of 3 components (surfactant, aqueous phase, and oil phase) corresponding to the region’s point within the diagram. The mass fractions $f_S$, $f_{AP}$, and $f_{PO}$ in the diagram were calculated by mass balance from the masses of each component obtained experimentally through...
the titration methodology. The titration consisted of fixing two component’s mass ratios and titrating a third component to reach a monophasic ternary mixture (blue region). The diagram indicates that the microemulsion region (Winsor IV or WIV) was reached.

![Figure 2. Ternary phase diagram.](image)

The region below the solubility curve (region in lilac) corresponds to a 3-component mixture with 2 or 3 phases. The mixture with 2 phases in this lilac region can be an oil-in-water (O/W) microemulsion in equilibrium with the excess oil phase (Winsor I or WI) or a water-in-oil (W/O) microemulsion in equilibrium with excess aqueous phase (Winsor II or WII). The presence of 3 phases corresponds to a microemulsion in equilibrium with an excess in the aqueous and oil phases (Winsor III or WIII). The yellow region corresponds to a partial miscibility between the surfactant and the oil phase. The three components’ mass ratio has not yet been sufficient to form a microemulsion.

A $2^k$ factorial design was used in the microemulsion area with four center points (central composite design) and axial points. Twelve microemulsion points were defined and used later in the drilling fluids’ formulation, when the influences of NP100 surfactant and pine oil on the filtrate volume and the formed filter-cake thickness were investigated.

2.2. Drilling Fluid Formulation

Initially, 12 drilling fluids were experimentally prepared. All drilling fluids presented in their composition the exact amounts of solid additives indicated in Table 1. The formulated drilling fluids only slightly differ from the microemulsion studied, composed of the surfactant NP100, pine oil, and the water-glycerol solution. The additives were included in the microemulsion at 10 min intervals, under intense agitation of 17,000 rpm, using a Hamilton Beach Fann Model HMD200 mixer (Hamilton Beach, Richmond, VA, USA).

| Table 1. Materials for drilling-fluids preparation. |
|---------------------------------|-----------------|-----------------|-----------------|-----------------|-----------------|-----------------|
| Microemulsion                  | CaCO$_3$        | Cloisite 20A Clay | HPA             | Xanthan Gum     | Barite          |
| 300 g                          | 10.0 g          | 4.0 g            | 1.0 g           | 1.0 g           | 80.0 g          |

2.3. Rheological Study

The drilling fluids were stirred for 5 min after 24 h from their preparation at 55 °C. Subsequently, the apparent-viscosity and plastic-viscosity parameters were determined. The apparent viscosity was calculated by dividing the reading at 600 rpm by 2, and the plastic viscosity by subtracting the reading at 600 rpm from the reading at 300 rpm. The
rheological experiments were carried out in a Fann Model 35-A viscometer (from Hamilton Beach, Glen Allen, VA, USA) according to API RP 13B-1 (American Petroleum Institute Recommended practice), 2017 [43]. After the fluid-loss tests, the filtrate’s viscosity for each fluid was evaluated using the Brookfield rheometer model DVIII ultra and a spindle-CP52 (Middleboro, MA, USA). The rheometer, coupled with a thermostatic bath and a computer, read the filtrate’s viscosities at 30 °C and 55 °C. The measurements were obtained automatically at each temperature, varying only the rotation speed. The Rheocalc Software provided, in tables, the viscosity readings.

2.4. Filtrate Volume

The filtrate volume was obtained through API fluid-loss test in an API filter press, in which a constant pressure of 100 psi was applied for 30 min with compressed air at room temperature, according to the standard API RP 13B-1 [43]. In total, 250 mL of the drilling fluid was used for the test. After 30 min, the filtrate volume was obtained. The test’s obtained values were used to apply the central composite design (CCD) and response surface methodology with the filtrate volume (FV) as the response variable.

2.5. Filter-Cake Thickness and Permeability

After the API fluid-loss tests, the filter medium—Whatman filter papers—was removed, and the filter-cake thickness (thkns) formed during the test was measured. Initially, the plates’ thicknesses (sides A, B, C, and D) were measured using a caliper (Figure 3).

Subsequently, the filter paper with the filter cake was placed between the two glass plates, and the thicknesses of the x, y, z, and w sides were measured. It was subtracted from the thickness of the y side, the sum of the side A’s thicknesses of plates 1 and 2, and the filter paper’s thickness, resulting in the filter-cake thickness on side A. This procedure was repeated for the other three sides (B, C, and D), and then the final filter cake’s thickness was calculated by the arithmetic mean of sides A, B, C, and D.

The filter cake’s permeability was then calculated using Darcy’s equation [44] for 100 psi and 30 min conditions [43], resulting in Equation (1):

\[ k = \frac{Q_f \times \varepsilon \times \mu}{8.95 \times 10^{-5}}, \]  

(1)
where \( k \) is the permeability (mD); \( Q_f \) is the filtrate volume (mL); \( \varepsilon \) is the filter-cake thickness (mm); and \( \mu \) is the filtrate’s viscosity (cP) at 30 °C and 55 °C.

3. Results and Discussion

Figure 4 shows the factorial points (rectangle in red) chosen at random, and the axial points (rectangle in blue) obtained with the factorial design method, considering the value of \( \alpha \), for two factors of 1.41. Central Composite Rotational Design (CCRD) was used for experimental design.

Table 2 shows the 12 microemulsion points in real and coded values of the surfactant (NP100), pine-oil, and aqueous-phase (water-glycerol) concentrations.

| Assay | X1 (Coded Surfactant Fraction) | X2 (Coded Oil Fraction) | Uncoded Surfactant Fraction | Uncoded Oil-Phase Fraction | Uncoded Aqueous-Phase Fraction |
|-------|-------------------------------|-------------------------|-----------------------------|---------------------------|-------------------------------|
| 1     | −1                            | −1                      | 0.450                       | 0.050                     | 0.500                         |
| 2     | +1                            | −1                      | 0.700                       | 0.050                     | 0.250                         |
| 3     | −1                            | +1                      | 0.450                       | 0.150                     | 0.400                         |
| 4     | +1                            | +1                      | 0.700                       | 0.150                     | 0.150                         |
| 5     | −1.41                         | 0                       | 0.400                       | 0.100                     | 0.500                         |
| 6     | +1.41                         | 0                       | 0.750                       | 0.100                     | 0.150                         |
| 7     | 0                             | −1.41                   | 0.575                       | 0.030                     | 0.400                         |
| 8     | 0                             | +1.41                   | 0.575                       | 0.170                     | 0.255                         |
| 9     | 0                             | 0                       | 0.575                       | 0.100                     | 0.325                         |
| 10    | 0                             | 0                       | 0.575                       | 0.100                     | 0.325                         |
| 11    | 0                             | 0                       | 0.575                       | 0.100                     | 0.325                         |
| 12    | 0                             | 0                       | 0.575                       | 0.100                     | 0.325                         |

Figure 4. Ternary diagram (NP100/Water-Glycerol/Pine Oil) with the delimited study region.

In this specific experimental design, there are 12 points, which were distributed into: factorial points, axial points (+\( \alpha \)) and (−\( \alpha \)), and central points (0). The factorial points correspond to levels (+1) and (−1). These levels indicate the highest and lowest values assumed by the independent variables. They are considered the basic levels and delimit the area in which the experimental model can be applied. The axial points are points that allow the estimation of quadratic terms in the model. These points allow the factorial design to be transformed into a composite central response surface design. The center points are repeated points represented by (0) and, when added to an experimental design, make it possible to identify if there is inflection (curvature) in the adjustment of the data.

Table 2 shows the 12 microemulsion points in real and coded values of the surfactant (NP100), pine-oil, and aqueous-phase (water-glycerol) concentrations.
3.1. Rheological Study

Table 3 presents the plastic-viscosity and apparent-viscosity data.

| Fluid | Plastic Viscosity (cP) | Apparent Viscosity (cP) |
|-------|------------------------|-------------------------|
| 1     | 97.0                   | 107.0                   |
| 2     | 115.0                  | 115.0                   |
| 3     | 81.0                   | 92.0                    |
| 4     | 118.0                  | 135.0                   |
| 5     | 115.0                  | 145.0                   |
| 6     | 121.0                  | 136.0                   |
| 7     | 130.0                  | 130.0                   |
| 8     | 95.0                   | 95.0                    |
| 9     | 125.0                  | 125.0                   |
| 10    | 127.5                  | 147.5                   |
| 11    | 125.0                  | 148.0                   |
| 12    | 130.5                  | 142.5                   |

Based on [43], the viscosity values obtained are in accordance with Petrobras N-2604 (1998), established by the American Petroleum Institute, whereby drilling fluids should present apparent and plastic viscosities greater than 15.0 cP and 4.0 cP, respectively. Furthermore, it can be said that the viscosity values (above 100 cP) are mainly due to the presence of glycerol and NP100 surfactant in significant quantities.

The drilling fluids were classified according to the Herschel–Bulkley model. The drilling fluids that follow this model have a solid structure below the yield stress, with very high viscosity and considerable initial resistance to flow. All drilling fluids had initial shear stress different from zero, and when reaching the limit yield stress, the fluid-structure broke, and a drop in viscosity could be observed. As the standard Fann-type viscometer does not take readings below 5.1 s\(^{-1}\) [45], an interpolation was performed to obtain the low-shear-yield point, \(\tau_0\). Figure 5 shows the flow curves for each drilling fluid along with their \(\tau_0\).

![Figure 5. Flow curves for the formulated drilling fluids.](image)

According to Figure 5, it is observed that for the same shear rate value (e.g., 500 s\(^{-1}\)), the shear stress values increased for some fluids. Thus, the same behavior was verified for fluids 5 and 7; 1, 3, and 8; and 2, 4, 6, and central points (9, 10, 11, and 12). The highest shear stress values were obtained for the fluids with the highest amounts of surfactant.
(2, 4, 6, and central points) (Table 2), as well as with the highest PV values (Table 3), probably due to long molecular chains of the NP100 that increased viscosity, as similarly verified in the study by Aftab et al. [28]. Fluids 1, 3, and 8 had intermediate shear stress values but with lower PV values. In this case, the fact that the amount of water in the fluid was more significant than that of oil, even with moderate amounts of surfactant, reduced the viscosity. Nonetheless, the microemulsion’s stability was maintained. Fluids 5 and 7, with similar amounts of surfactant and water in their formulations, had lower shear stress values. Still, due to a significant amount of surfactant in these formulations, the PV was also high.

3.2. Filtrate Volume

Table 4 presents the obtained filtrate-volume ($F_V$) values. It is observed that all of them are less than 15 mL, following [43], established by the American Petroleum Institute.

| Assay | Surfactant | Pine Oil | $F_V$ (mL) |
|-------|------------|----------|------------|
| 1     | 0.450      | 0.050    | 1.3        |
| 2     | 0.700      | 0.050    | 2.8        |
| 3     | 0.450      | 0.150    | 3.7        |
| 4     | 0.700      | 0.150    | 8.5        |
| 5     | 0.400      | 0.100    | 2.0        |
| 6     | 0.750      | 0.100    | 6.1        |
| 7     | 0.575      | 0.030    | 4.0        |
| 8     | 0.575      | 0.170    | 12.4       |
| 9     | 0.575      | 0.100    | 10.4       |
| 10    | 0.575      | 0.100    | 9.8        |
| 11    | 0.575      | 0.100    | 10.1       |
| 12    | 0.575      | 0.100    | 9.9        |

Analyzing Table 4, as the surfactant or pine-oil mass fraction increases, there is also an increase in the filtrate volume, with the oil phase being the most influential component. This may occur because the NP100 surfactant has a hydrophilic–lipophilic balance (HLB) equal to 13, is more soluble in water, and, consequently, less soluble in the oil phase. As a result, it favors the formulated drilling-fluid solid particles’ interaction with the aqueous phase (microemulsion O/W). Thus, it is expected that drilling fluids with less oil phase in their composition present a lower fluid loss.

Murtaza et al. [46] studied the behavior of filtrate loss using quaternary ammonium dicationic surfactant with phenyl linker to minimize clay-swelling problems, severely affecting wellbore stability and obtaining an increase in the average filtrate volume, reaching 19, 10 mL and 18 mL. These data are consistent with the found results, in which the filtrate volume increases with the addition of NP100 surfactant to the microemulsion composition. However, it is worth noting that the highest filtrate-volume value obtained is still acceptable and within the norms.

Paul and Adewale [47] used Zirconium (IV) oxide ($\text{ZRO}_2$) nanoparticles as additives for WBDM and had average values of 5 mL at 27°C. In this work, in terms of filtrate volume, the microemulsified base per se provided similar values. With the significant increase in temperature (120°C), [46] averaged 12 mL for the filtrate volume, indicating that the drilling fluids remained within API standards. It can be considered that microemulsified bases are thermally stable, and it is expected that similar results may be obtained under HPHT (high pressure high temperature) conditions, as they remain stable/homogeneous above 55°C, which is the average temperature of some oil reservoirs [19,35,41].

3.3. Filter-Cake Thickness and Permeability

In order to calculate the permeability, the mud filtrate’s viscosity was measured at 30°C and 55°C. Table 5 presents the resulting viscosity of the filtrate at both temperatures and the thickness and permeability of the filter cake.
Table 5. Thickness (thkns), mud filtrate’s viscosity (cP), and permeability of the formed filter cake at 30 °C and 55 °C.

| Drilling Fluid | Thickness (mm) | Filtrate Viscosity (cP) 30 °C | Filtrate Viscosity (cP) 55 °C | Permeability (mD) 30 °C | Permeability (mD) 55 °C |
|----------------|----------------|-------------------------------|-------------------------------|-------------------------|-------------------------|
| 1              | 0.92           | 25.35                         | 13.56                         | 6.26 × 10⁻³             | 3.35 × 10⁻³             |
| 2              | 0.76           | 47.68                         | 21.96                         | 7.78 × 10⁻³             | 3.58 × 10⁻³             |
| 3              | 0.64           | 25.99                         | 8.06                          | 3.57 × 10⁻³             | 1.11 × 10⁻³             |
| 4              | 0.74           | 69.43                         | 1.84                          | 12.9 × 10⁻³             | 2.57 × 10⁻³             |
| 5              | 1.24           | 41.56                         | 1.17                          | 22.1 × 10⁻³             | 5.42 × 10⁻³             |
| 6              | 0.76           | 40.08                         | 1.51                          | 10.4 × 10⁻³             | 2.72 × 10⁻³             |
| 7              | 0.64           | 27.14                         | 1.34                          | 5.29 × 10⁻³             | 3.38 × 10⁻³             |
| 8              | 0.95           | 57.08                         | 1.86                          | 27.2 × 10⁻³             | 5.17 × 10⁻³             |
| 9              | 0.90           | 60.62                         | 1.77                          | 13.7 × 10⁻³             | 3.33 × 10⁻³             |
| 10             | 0.77           | 72.32                         | 1.35                          | 18.9 × 10⁻³             | 3.50 × 10⁻³             |
| 11             | 0.80           | 70.55                         | 1.08                          | 18.2 × 10⁻³             | 3.63 × 10⁻³             |
| 12             | 0.98           | 51.51                         | 1.61                          | 11.7 × 10⁻³             | 2.65 × 10⁻³             |

From Table 5, it is possible to understand that as the surfactant or pine-oil mass fraction increases, there is also an increase in the filter-cake thickness, with the surfactant being the most influential component. The tests corresponding to fluids 1, 2, 3, 5, and 7 provided lower thickness values than the other tests. This result is consistent with the filtrate volumes obtained (Table 4) since the surfactant interaction with the aqueous phase reduced the fluid loss and favored the formation of a thinner filter cake.

The desirable filter cake for drilling activities should be as thin and waterproof as possible. The thicknesses obtained can be considered acceptable, as they presented low values similar to those obtained by Bageri et al. [18]. An average of 1.4 mm was obtained by [46], who studied the addition of the quaternary ammonium dicationic surfactant. The results obtained are within the expected values for discarding operational problems in the wellbore, suggesting that the average thickness obtained in this work is acceptable.

All drilling fluids showed good permeability results. These results can be compared to [7], who obtained an average of 0.026 mD. At the highest temperature (55 °C), the average permeability is even lower, implying good permeability performance of the fluids formulated at the well’s operating temperature. All values obtained are considered adequate by [48].

3.4. Statistical Analysis: Filtrate Volume

Table 6 presents the effects of the regression statistics on the filtrate volume as a response variable.

Table 6. Estimation of effects on filtrate volume.

| R² = 0.936 | Efect | Std. Err. | p-Value | Coefficient | Std. Err. Coef. | −95% Inf. | +95% Sup. |
|------------|-------|-----------|---------|-------------|-----------------|-----------|-----------|
| Fator/ Interc | 10.05 | 0.66      | 5.00 × 10⁻⁶ | 10.05 | 0.66 | 8.44 | 11.65 |
| Surf (L) | 3.02 | 0.93 | 1.76 × 10⁻² | 1.51 | 0.47 | 0.37 | 2.65 |
| Surf (S) | −7.02 | 1.04 | 5.20 × 10⁻⁴ | −3.51 | 0.52 | −4.79 | −2.23 |
| PO (L) | 4.99 | 0.93 | 1.73 × 10⁻³ | 2.50 | 0.46 | 1.36 | 3.63 |
| PO (S) | −2.88 | 1.04 | 3.29 × 10⁻² | −1.43 | 0.52 | −2.71 | −0.16 |
| Surf × PO | 1.65 | 1.31 | 2.57 × 10⁻¹ | 0.82 | 0.66 | −0.78 | 2.43 |

Surf is the surfactant concentration; PO is the pine-oil concentration; (L) represents the linear term; (S) represents the quadratic term; and Surf × PO is the interaction of the independent variables.

According to Table 6, the factors were statistically significant, except for the surfactant interaction with pine oil (Surf × PO = 2.57 × 10⁻¹), since the p-value must be less than 0.05.
The $R^2$ value was 0.936. Equation (2) presents the obtained model for the filtrate volume in coded variables.

$$V_f = 10.05 + 1.51\text{Surf} + 2.50\text{PO} - 3.51\text{Surf}^2 - 1.43\text{PO}^2,$$

In order to use the real concentration values $X_1$ and $X_2$, shown in Table 2, it is necessary to use the equation for converting real variables to coded variables. It is important to note that the model obtained is found in coded variables (Surf and PO). Therefore, Equations (3) and (4) give the conversion equations for surfactant and pine oil.

$$\text{Surf} = \frac{X_1 - 0.575}{0.125},$$

$$\text{PO} = \frac{X_2 - 0.10}{0.05}.$$

Table 7 presents the ANOVA (Analyses of Variance) results for the model obtained from the filtrate volume.

| Variation Source | Degrees of Freedom | Sum of Squares | Mean Square | Statistics F | $p$-Value |
|------------------|--------------------|----------------|-------------|--------------|-----------|
| Surf (L)         | 1                  | 18.30          | 18.29       | 10.52        | $1.76 \times 10^{-2}$ |
| Surf (S)         | 1                  | 78.96          | 78.96       | 45.41        | $5.20 \times 10^{-4}$ |
| PO (L)           | 1                  | 49.89          | 49.89       | 28.69        | $1.73 \times 10^{-3}$ |
| PO (S)           | 1                  | 13.22          | 13.22       | 7.60         | $3.29 \times 10^{-2}$ |
| Surf $\times$ PO | 1                  | 2.72           | 2.72        | 1.56         | $2.57 \times 10^{-1}$ |
| Residual         | 6                  | 10.43          | 1.74        |              |           |
| Total            | 11                 | 163.91         |             | 23.05        |           |

For a 95% confidence interval ($\alpha = 0.05$), the theoretical F value was compared with the model’s calculated F value. Theoretical F value was determined considering the model’s degrees of freedom and the residual as 4 and 6, respectively. The theoretical F value was 4.53. Since the calculated F value (23.05) is greater than the theoretical F, it verifies the model’s statistical significance. The response surface obtained for the filtrate-volume model is shown in Figure 6.

Figure 6. Response surface: filtrate volume.
It can be seen in Figure 6 that the filtrate volume increases as the concentrations of pine oil and surfactant approach the central point. This region corresponds to the maximum concentration of pine oil and a medium concentration of surfactant: approximately 57.5% surfactant, 15% oil phase, and 27.5% aqueous phase. Conversely, the lowest filtrate volume corresponds to approximately 45% surfactant, 5% pine oil, and 50% aqueous phase.

3.5. Statistical Analysis: Filter-Cake Thickness

Table 8 presents the results of the effects with the regression statistics for thickness as the response variable.

Table 8. Estimation of effects on the filter-cake thickness.

| Effect          | Std. Err. | p     | Coefficient | Std. Err. Coef. | -95% Inf | +95% Sup |
|-----------------|-----------|-------|-------------|-----------------|----------|----------|
| Factor/Interc   | 0.74      | 0.04  | $8.20 \times 10^{-7}$ | 0.74            | 0.04     | 0.66     | 0.83     |
| Surf (L)       | 0.42      | 0.05  | $1.70 \times 10^{-4}$ | 0.21            | 0.03     | 0.15     | 0.27     |
| Surf (S)       | -0.03     | 0.06  | $6.09 \times 10^{-1}$ | -0.02           | 0.03     | -0.08    | 0.05     |
| PO (L)         | 0.17      | 0.05  | $3.78 \times 10^{-2}$ | 0.09            | 0.03     | 0.03     | 0.15     |
| PO (S)         | 0.00      | 0.06  | $9.58 \times 10^{-1}$ | 0.00            | 0.03     | -0.07    | 0.07     |
| Surf × PO      | 0.25      | 0.07  | $1.36 \times 10^{-2}$ | 0.12            | 0.04     | 0.04     | 0.21     |

Surf is the surfactant concentration; PO is the pine-oil concentration; (L) represents the linear term; (S) represents the quadratic term, and Surf × PO is the interaction of the independent variables.

It was found that the mass-fraction-quadratic terms of the surfactant and the pine oil were not significant, as the p-value was greater than 0.05. In addition, the model’s $R^2$ value was 0.94, thus indicating that the data adjusted satisfactorily to the model. Equation (5) presents the thickness model in coded variables.

$$Thkns = 0.74 + 0.21\text{Surf} + 0.09\text{PO} + 0.12\text{Surf} \times \text{PO},$$

Similarly to the filtrate-volume model, it is necessary to use Equations (4) and (5) to convert the real values into coded ones.

Table 9 presents the ANOVA results for the model obtained from the thickness.

Table 9. ANOVA: Filter-cake thickness.

| Variation Source | Degrees of Freedom | Sum of Squares | Mean Square | Statistics F | p-Value |
|------------------|--------------------|----------------|-------------|--------------|---------|
| Surf (L)         | 1                  | 0.35           | 0.35        | 68.23        | $1.70 \times 10^{-4}$ |
| Surf (S)         | 1                  | 0.00           | 0.00        | 0.29         | $6.09 \times 10^{-1}$ |
| PO (L)           | 1                  | 0.06           | 0.06        | 11.90        | $1.37 \times 10^{-2}$ |
| PO (S)           | 1                  | 0.00           | 0.00        | 0.00         | $9.58 \times 10^{-1}$ |
| Surf × PO        | 1                  | 0.06           | 0.06        | 11.90        | $1.36 \times 10^{-2}$ |
| Residual         | 6                  | 0.03           | 0.01        | 30.67        |         |
| Total            | 11                 | 0.51           |             |              |         |

The model’s F-value was calculated disregarding the quadratic terms, which were not significant. The degrees of freedom of the model and the residues were 3 and 6, respectively. The theoretical F value is 4.76. The calculated F value (30.67) being higher than the theoretical F, showing the model’s statistical significance.

The response surface obtained for the thickness model is shown in Figure 7.

It can be seen from Figure 7 that the surfactant’s influence on the filter-cake thickness is greater than the pine oil’s influence. This is because the maximum point corresponds to 70% surfactant, 15% pine oil, and 15% aqueous phase, while the minimum is obtained in approximately 45% surfactant, 15% pine oil, and 40% aqueous phase.
Table 9. ANOVA: Filter-cake thickness.

| Variation Source | Degrees of Freedom | Sum of Squares | Mean Square | Statistics F | p-Value |
|------------------|--------------------|----------------|-------------|--------------|---------|
| Surf (L)         | 1                  | 0.35           | 0.35        | 68.23        | 1.70 × 10^{-4} |
| Surf (S)         | 1                  | 0.00           | 0.00        | 0.29         | 6.09 × 10^{-1} |
| PO (L)           | 1                  | 0.06           | 0.06        | 11.90        | 1.37 × 10^{-2} |
| PO (S)           | 1                  | 0.00           | 0.00        | 0.00         | 9.58 × 10^{-1} |
| Surf × OPO       | 1                  | 0.06           | 0.06        | 11.90        | 1.36 × 10^{-2} |
| Residual         | 6                  | 0.03           | 0.01        |              |         |
| Total            | 11                 | 0.51           | 30.67       |              |         |

The model's F-value was calculated disregarding the quadratic terms, which were not significant. The degrees of freedom of the model and the residues were 3 and 6, respectively. The theoretical F value is 4.76. The calculated F value (30.67) being higher than the theoretical F, showing the model's statistical significance.

The response surface obtained for the thickness model is shown in Figure 7.

Figure 7. Response surface: filter-cake thickness.

It can be seen from Figure 7 that the surfactant's influence on the filter-cake thickness is greater than the pine oil's influence. This is because the maximum point corresponds to 70% surfactant, 15% pine oil, and 15% aqueous phase, while the minimum is obtained in approximately 45% surfactant, 15% pine oil, and 40% aqueous phase.

3.6. Model Interpretation

Taking the response surfaces (Figures 6 and 7) and comparing them, it is possible to see that the minimum points are divergent. However, the models provide adequate information to determine the best operating condition.

The point with 45% surfactant, 15% pine oil, and 40% aqueous phase minimizes the filter-cake thickness and produces filtrate-volume values close to 6 mL. On the other hand, the point with 45% surfactant, 5% pine oil, and 50% aqueous phase does not minimize the thickness but provides a low value (<0.6 mm) and minimizes the filtrate-volume value (<2 mL). The best operational point minimizes the filtrate volume, as it will provide a good thickness value and ensure that drilling fluids formulated in this condition present less risk of differential sticking and fluid loss.

According to the experimental models obtained, the best performance of the microemulsified system (NP100/Pine Oil/Water-Glycerol) occurs with a smaller composition of surfactant or pine oil, which implies that the aqueous phase is in abundance in the system; and these results are consistent with the hydrophilic nature of the NP100 surfactant. Therefore, a dilution in water in these drilling fluids should favor the microemulsified system's interaction, expecting promising results for the filtrate volume and filter-cake thickness.

It is still possible to state that compositions on the right side of Figure 3, that is, high compositions of pine oil and surfactant, will result in drilling fluids that will not meet the minimum specifications. This fact is due to the hydrophilic character of the NP100 surfactant will result in an unstable microemulsion system.

4. Conclusions

In order to verify the influence of the nonionic surfactant (NP100) and vegetable oil (pine oil) on the formation of the filter-cake and filtrate volume of microemulsion-based drilling fluids, the following conclusions may be drawn:

- The formulated drilling fluids had a sufficient filtrate volume (1.3 mL to 12.4 mL), being within the norms’ standards (<15 mL);
- The microemulsion point corresponding to 45% surfactant and 5% pine oil obtained the lowest filtrate volume (1.3 mL);
- The microemulsion points corresponding to 45% surfactant and 15% pine oil (fluid 3) and 57.7% surfactant and 3% pine oil (fluid 7) obtained the thinner filter cakes, producing a thickness of 0.64 mm.
• The permeabilities obtained for all drilling fluids are within the expected range, which is less than 0.027 mD, being considered low and ideal.
• The results obtained from filter cake, filtrate volume, and permeability for all formulated drilling fluids were satisfactory, as they presented values within the range stipulated by the standards. Thereby, it can be concluded that fluid 3 (45% surfactant and 15% pine oil) is the most promising of the fluids formulated on a laboratory scale, as it will provide good results for all response variables.
• This study also verified that it is possible to obtain microemulsion-based drilling fluids formulated from biodegradable and environmentally acceptable components, with good prospects for field-scale applications.

5. Recommendations for Future Research
• Carry out HPHT evaluation of the formulated fluids, even if the microemulsions have sufficient thermal stability to be applied in wellbores with temperatures above 55 °C.
• Check the influence of salts, such as NaCl and KCl, on the stability of the microemulsions used, the filtrate volume, and filter-cake thickness.

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References
1. Burgoyne, A.T., Jr.; Millheim, K.K.; Chenevert, M.E.; Young, F.S., Jr. Applied Drilling Engineering, 1st ed.; SPE Textbooks Series vol. 2; Society of Petroleum Engineers: Richardson, TX, USA, 1986.
2. Cunha, J.C.; Kastor, R. Introduction to rotary drilling. In Fundamentals of Drilling Engineering, 1st ed.; Mitchell, R.F., Miska, S.Z., Eds.; Society of Petroleum Engineers: Richardson, TX, USA, 2011; Volume 12, pp. 15–55.
3. Hossain, M.E.; Islam, M.R. Drilling Engineering Problems and Solutions: A Field Guide for Engineers and Students, 1st ed.; Wiley: Beverly, MA, USA, 2018; pp. 12–75.
4. Bridges, S.; Robinson, L. A Practical Handbook for Drilling Fluids Processing, 1st ed.; Elsevier: Houston, TX, USA, 2020; pp. 139–161.
5. Etehadi, A.; Altun, G. Functional and practical analytical pressure surge models through Herschel Bulkley fluids. J. Pet. Sci. Eng. 2018, 171, 748–759. [CrossRef]
6. Vryzas, Z.; Kelessidis, V.C. Nano-based drilling fluids: A review. Energies 2017, 10, 540. [CrossRef]
7. Vipulanandan, C.; Mohammed, A. Effect of drilling mud bentonite contents on the fluid loss and filter cake formation on a field clay soil formation compared to the API fluid loss method and characterized using Vipulanandan models. J. Pet. Sci. Eng. 2020, 189, 107029. [CrossRef]
8. Aird, P. Deepwater Drilling: Well Planning, Design, Engineering, Operations, and Technology Application, 1st ed.; Elsevier: Cambridge, MA, USA, 2018.
9. Civin, F. Reservoir Formation Damage, 2nd ed.; Gulf Professional Publishing: Houston, TX, USA, 2007.
10. Ezeakacha, C.P.; Salehi, S. Experimental and statistical investigation of drilling fluid loss in porous media: Part 2 (Fractures). J. Nat. Gas Sci. Eng. 2019, 65, 257–266. [CrossRef]
11. Okoro, E.E.; Dosunmu, A.; Iyuke, S. Silicon Ethoxide as reversible surfactant in reversible drilling mud and the mu’s effect on permeability. J. King Saud Univ. Eng. Sci. 2019, 32, 402–406. [CrossRef]
12. Caen, R.; Darley, H.C.H.; Gray, G.R. Drilling Fluids and Complementation, 6th ed.; Elsevier: Rio de Janeiro, Brazil, 2014.
13. Darley, H.C.H.; Gray, G.R. Composition and Properties of Drilling and Completion Fluids, 5th ed.; Gulf Publishing Company: Houston, TX, USA, 1988.
14. You, L.; Tan, Q.; Kang, Y.; Zhang, X.; Xu, C.; Lin, C. Optimizing the particle size distribution of drill-in fluids based on fractal characteristics of porous media and solid particles. J. Nat. Gas Sci. Eng. 2018, 171, 1223–1231. [CrossRef]
15. Menezes, R.R.; Marques, L.N.; Campos, L.A.; Ferreira, H.S.; Santana, L.N.L.; Neves, G.A. Use of statistical design to study the influence of CMC on the rheological properties of bentonite dispersions for water-based drilling fluids. *Appl. Clay Sci.* 2010, 49, 13–20. [CrossRef]

16. Gamal, H.; Elkatatny, S.; Abdulraheem, A. Effect of the filtrate fluid of water-based mud on sandstone rock strength and elastic moduli. *ACS Omega* 2020, 5, 32677–32688. [CrossRef]

17. Chesser, B.G.; Clark, D.E.; Wise, W.V. Dynamic and static filtrate-loss techniques for monitoring filter-cake quality improves drilling-fluid performance. *SPE Drill. Compl.* 1994, 9, 189–192. [CrossRef]

18. Bageri, B.S.; Adebayo, A.R.; Al Jaberi, J.; Patil, S. Effect of perlite particles on the filtration properties of high-density barite weighted water-based drilling fluid. *Powder Technol.* 2020, 360, 1157–1166. [CrossRef]

19. Curbelo, F.D.S.; Caminha, T.T.; Garnica, A.I.C.; Melo, G.N.A.; Araújo, E.A.; Freitas, J.C.O. Microemulsion-based flushing fluid for effective removal of filter cake in wells cementation. *Braz. J. Pet. Gas* 2019, 13, 119–127. [CrossRef]

20. Farias, K.V.; Amorim, L.V.; Ferreira, H.C.; Pereira, E. Study of rheology and filter-cake thickness of drilling fluids: Influence of anionic dispersants and surfactant. *Cerâmica* 2006, 52, 307–314. [CrossRef]

21. Schulman, J.H.; Hoar, T.P. Transparent water-in-oil dispersions: The oleopathic hydromicelle. *Nature* 1943, 152, 102–103. [CrossRef]

22. Langevin, D. *Emulsions, Microemulsions and Foams*; 1st ed.; Butherworth & Co.: London, UK, 1954.

23. Winsor, P.A. *Solvent Properties of Amphiphilic Compounds*; 1st ed.; Springer: Cham, Switzerland, 2020; pp. 71–95.

24. Najjar, R. Microemulsions—A brief introduction. In *Microemulsions An Introduction to Properties and Applications*, 1st ed.; Najjar, R., Ed.; InTech: Rijeka, Croatia, 2012; pp. 3–11.

25. Hayes, J.B.; Haws, G.W.; Gogarty, W.B. Water-In-Oil Microemulsion Drilling Fluids. U.S. Patent 4,012,329, 15 March 1977.

26. Farias, K.V.; Amorim, L.V.; Ferreira, H.C.; Pereira, E. Study of rheology and filter-cake thickness of drilling fluids: Influence of anionic dispersants and surfactant. *Cerâmica* 2006, 52, 307–314. [CrossRef]

27. Foust, A.S.; Wenzel, L.A.; Clump, C.W.; Maus, L.; Andersen, L.B. Synthesis and application of the drilling mud additive in the presence of non-ionic surfactants. *ACS Omega* 2020, 5, 11224–11243. [CrossRef]

28. Aftab, A.; Ali, M.; Sahito, M.F.; Mohanty, U.S.; Jha, N.K.; Akhondzadeh, H.; Azhar, M.R.; Ismail, A.R.; Keshavarz, A.; Igliaver, S. Environmental friendliness and high performance of multifunctional Tween 80/ZnO-nanoparticles-added water-based drilling fluid: An experimental approach. *ACS Sustain. Chem. Eng.* 2020, 8, 11224–11243. [CrossRef]

29. Yunita, P.; Irawan, S.; Kania, D. Optimization of water-based drilling fluid using non-ionic and anionic surfactant additives. *Procedia Eng.* 2016, 148, 1184–1190. [CrossRef]

30. Sabeghalvoa, M.; Sabbaghi, S.; Afsharimoghadam, P. Synthesis and application of the drilling mud additive in the presence of anionic and nonionic surfactants. *Int. J. Nano Dimens.* 2016, 7, 321–328. [CrossRef]

31. Numkam, G.L.; Akbari, B. Effect of surfactant chemistry on drilling mud performance. *J. Pet. Sci. Eng.* 2019, 174, 1309–1320. [CrossRef]

32. Saboori, R.; Sabaghi, S.; Kalantariasl, A.; Mowlad, D. Improvement in filtration properties of water-based drilling fluid by nanocarboxymethyl cellulose/polystyrene core-shell nanocomposite. *J. Pet. Explor. Prod. Technol.* 2018, 8, 445–454. [CrossRef]

33. Aftab, A.; Ismail, A.R.; Ibupoto, Z.H.; Akeiber, H.; Malghani, M.G.K. Nanoparticles based drilling muds a solution to drill effective removal of filter cake in wells cementation. *Energies* 2021, 14, 4965. [CrossRef]
45. Power, D.; Zamora, M. Drilling fluid yield stress: Measurement techniques for improved understanding of critical drilling fluid parameters. In Proceedings of the AADE Technical Conference, Houston, TX, USA, 1–3 April 2003.

46. Murtaza, M.; Kamal, M.S.; Hussain, S.S.; Mahmoud, M.; Syed, N.A. Quaternary ammonium gemini surfactants having different spacer length as clay swelling inhibitors: Mechanism and performance evaluation. *J. Mol. Liq.* 2020, 308, 113054. [CrossRef]

47. Paul, A.A.L.; Adewale, F.J. Experimental investigation of fluid loss and cake thickness control ability of zirconium (IV) oxide (Z_R O_2) nanoparticles in water based drilling mud. *Int. J. Eng. Technol.* 2018, 7, 702–707. [CrossRef]

48. Jiao, D.; Sharma, M.M. Investigation of Dynamic Mud Cake Formation: The Concept of Minimum Overbalance Pressure. In Proceedings of the SPE Annual Technical Conference and Exhibition, Houston, TX, USA, 3 October 1993. [CrossRef]