Formation of the Mg II h and k Polarization Profiles in a Solar Plage Model and Their Suitability to Infer Magnetic Fields

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Abstract

The Mg II h and k lines are among the strongest in the near-ultraviolet solar spectrum and their line core originates in the upper chromosphere, just below the transition region. Consequently, they have become one of the main targets for investigating the magnetism of the upper solar atmosphere. The recent Chromospheric Layer Spectropolarimeter (CLASP2) mission obtained unprecedented spectropolarimetric data on these lines in an active region plage, which have already been used to infer the longitudinal component of the magnetic field by applying the weak-field approximation. In this paper, we aim at improving our understanding of the diagnostic capabilities of these lines by studying the emergent Stokes profiles resulting from radiative transfer calculations in a radiative magnetohydrodynamic time-dependent model representative of a solar plage. To this end, we create a synthetic observation with temporal and spatial resolutions similar to those of CLASP2. We find strong asymmetries in the synthetic profiles of circular polarization, which considerably complicate the application of the weak-field approximation. We demonstrate that the selective application of the weak-field approximation to fit different spectral regions in the profile allows us to retrieve information about the longitudinal component of the magnetic field in different regions of the model atmosphere, even when the circular polarization profiles are not antisymmetric and are formed in the presence of strong velocity and magnetic field gradients.

Unified Astronomy Thesaurus concepts: Spectropolarimetry (1973); Solar chromosphere (1479); Solar magnetic fields (1503); Solar transition region (1532)

1. Introduction

The determination of the magnetic fields in the outer layers of the solar atmosphere is one of the main challenges in solar physics nowadays and a key requirement for their physical understanding (e.g., the review by Trujillo Bueno & del Pino Alemán 2022). In the outer solar atmosphere (i.e., upper chromosphere, transition region, and corona) the density of the solar plasma is low enough for the magnetic pressure to dominate over the plasma pressure ($\beta \ll 1$, Priest 2014), and thus the behavior of this plasma is determined by the magnetic field. Empirical knowledge of the magnetic field is thus key to understanding some of the energetic processes that take place in the outer solar atmosphere, such as solar flares or the heating of the solar corona to several million kelvin.

Atomic spectral lines encode information about the physical properties of the plasma from the regions in the atmosphere where they are formed. In particular, their polarization profiles carry information about the strength and orientation of the magnetic field. While most of the atomic lines observed in the visible and infrared solar spectrum originate in the photosphere and lower chromosphere, a number of them that originate in the upper chromosphere and transition region are resonance lines found in the ultraviolet (UV) solar spectrum (see the review of Trujillo Bueno et al. 2017). In some of these spectral lines, different spectral regions originate at different heights in the atmosphere due to changes in the opacity; a particular case is the Mg II h and k resonant doublet. While the h and k line centers are formed in the upper chromosphere, near the base of the transition region, their wings originate in the lower layers of the chromosphere. Consequently, the Mg II h and k doublet is one of the best tools to study both atmospheric regions simultaneously.

By studying the polarization profiles of resonance lines in the UV and, in particular, the fingerprints that the magnetic field introduces on the spectral line polarization, we can thus aim at uncovering the magnetic fields of the upper solar chromosphere. There are two key effects induced by the magnetic field, namely, the Hanle and the Zeeman effects. The Hanle effect is the magnetic modification of the scattering polarization in the core of spectral lines, which in turn is a consequence of the radiatively induced population imbalances and coherence between the magnetic sublevels of the line’s atomic levels (the so-called atomic level polarization). The Zeeman effect is the energy splitting of the degenerate magnetic sublevels of an atomic level and, in turn, of the magnetic components of a spectral line, resulting in spectral line polarization (e.g., Landi Degl’Innocenti & Landolfi 2004). The two effects of course coexist, and their joint action results in the magnetic sensitivity of the scattering polarization in the core and the wings of spectral lines via the Hanle and magnetooptical effects, respectively (see Alsina Ballester et al. 2016; del Pino Alemán et al. 2016).

Significant challenges, both observational and theoretical, are faced when trying to exploit these capabilities of the UV atomic lines to infer the magnetic field in the upper chromosphere. UV observations are impossible from ground-based facilities due to the large opacity of the Earth’s atmosphere at these wavelengths. Consequently, space telescopes are necessary to observe the Sun at those wavelengths. The first
opportunity to study the solar Mg II h and k lines came with the Ultraviolet Spectrometer and Polarimeter (UVSP, Calvert et al. 1979; Woodgate et al. 1980) aboard the Solar Maximum Mission (SMM, Bohlin et al. 1980). This mission provided the first polarimetric data for the Mg II h and k doublet from a quiet region near the solar limb and showed the first signatures of significant scattering polarization in the far wings of these lines (Henze & Stenflo 1987; Manso Sainz et al. 2019). For some years now the Interface Region Imaging Spectrograph (IRIS, De Pontieu et al. 2014) has provided systematic observations of the intensity in some UV atomic lines (Mg II h and k lines among them). Recently, the Chromospheric Layer Spectropolarimeter (CLASP2, Narukage et al. 2016) suborbital mission, launched in 2019, achieved unprecedented spectropolarimetric observations of Mg II h and k lines in a quiet region near the solar limb and in a plage region. These data allowed us to determine, for the first time, the longitudinal component of the magnetic field at several heights going from the upper photosphere to the upper chromosphere in a plage region (Ishikawa et al. 2021). The theoretical and numerical modeling of these strong resonance UV lines is challenging because of all the physical processes involved in their formation. Due to the relatively low density in the higher layers of the chromosphere and the subsequent lower rate of collisional processes, the Mg II h and k lines form out of thermodynamic equilibrium (i.e., in nonlocal thermodynamic equilibrium, NLTE). Moreover, the frequency correlation between the absorbed and the re-emitted photons in scattering processes becomes a key ingredient in the line formation, the so-called partial frequency redistribution (PRD) effects (Milkey & Mihalas 1974; Uitenbroek 1997). The formation of the intensity of these lines has also been studied in detail in relatively realistic model atmospheres resulting from 3D radiative magnetohydrodynamic (rMHD) simulations accounting for 3D radiative transfer (RT) (Leenaarts et al. 2013a, 2013b) and in flare models (Kerr et al. 2019a, 2019b). Moreover, when modeling the polarization of these lines, it is also necessary to account for J-state interference between the upper levels of the two transitions (Belluzzi & Trujillo Bueno 2012; del Pino Alemán et al. 2016, 2020).

In this work, we study the formation of the Stokes profiles of the Mg II h and k lines in a rMHD simulation representative of a solar plage region and study the suitability of the weak-field approximation (WFA) to study the magnetism of the solar chromosphere; we support the results recently presented by Ishikawa et al. (2021). In Section 2 we describe the theoretical problem and the atomic and atmospheric models used in this work. We present the results in Section 3. We describe some representative Stokes profiles resulting from 1.5D radiative transfer calculations, commenting on the sensitivity of the Stokes profiles to the thermal, dynamic, and magnetic properties along the line of sight (LOS). Next, we imitate an observation by degrading our results to the spatial and temporal resolution of the CLASP2 observations. We study the resulting profile and compare it with available observations. Using this synthetic observation we demonstrate the applicability of the weak-field approximation to the circular polarization profiles of the Mg II h and k lines to determine the longitudinal component of the magnetic field even when strong gradients in velocity and magnetic field are present in the line formation region. Finally, in Section 5 we present our main conclusions.

2. Formulation of the Problem

We study the intensity and polarization profiles of the Mg II h and k doublet and its subordinate triplet in a 2.5D magnetohydrodynamic atmospheric model representative of a solar plage region, including its temporal evolution for 700 s, with 10 s cadence (see Martinez-Sykora et al. 2020). With this purpose, we solve the nonlocal and nonlinear 1.5D RT problem with polarization in an rMHD model. The RT calculations, performed column by column as if they were plane-parallel model atmospheres, take into account NLTE effects, scattering polarization, PRD effects, J-state interference in the presence of magnetic fields of arbitrary strength (incomplete Paschen–Back regime), and the Doppler shifts produced by the model’s macroscopic velocities. The solution of this RT problem requires the joint solution of the statistical equilibrium equations governing the atomic population and quantum coherence and the RT equations describing absorption and emission processes as the polarized light travels through the solar atmosphere (Landi Degl’Innocenti & Landolfi 2004). PRD effects are included following the formalism of Casini et al. (2014, 2017a, 2017b). The RT problem has been solved using the HanleRT code described in del Pino Alemán et al. (2016, 2020).

The only 3D RT code publicly available today for modeling the polarization of spectral lines without assuming LTE (Stépán & Bueno 2013) is not able to account for all the physical ingredients needed for the modeling of the polarization of the Mg II h and k lines, namely PRD and J-state interference in the presence of magnetic fields of arbitrary strength. While accounting for 3D RT may have an impact on the formation of the Mg II h and k lines, currently it has only been possible to study the effect of horizontal radiation transfer on the intensity profiles (Sukhorukov & Leenaarts 2017). These authors concluded that, when comparing horizontal transfer and PRD effects, the latter are significantly more important for disk-center lines of sight. Moreover, including the horizontal component of the macroscopic velocity allows us to qualitatively account for the lack of axial symmetry inducing linear polarization in 3D model atmospheres (Jaume Bestard et al. 2021). Besides, it is important to note that the considered 2.5D model atmosphere already includes a plane of symmetry that affects the linear polarization and that does not represent the real solar atmosphere. In summary, regarding the main object of study in this paper, namely the fractional circular polarization for the disk-center line of sight, we do not expect a significant impact due to the effects of horizontal RT, nor that it would affect our conclusions.

Theoretical studies (e.g., Sampoorna et al. 2017) recommend to take into account the angle-dependent frequency redistribution to model the linear polarization of the spectral line, especially in the presence of a magnetic field. However, the intricate vertical stratification in the columns of the model atmosphere, the need to account for nonaxial symmetry due to the presence of nonvertical velocities and magnetic fields, and the amount of calculation that needs to be performed in order to cover an adequate spatial fraction of the model in enough time, results in computing time requirements that are unfeasible at this moment. Consequently, the calculations have been carried out using the angle-averaged approximation (Mihalas 1978; Belluzzi & Trujillo Bueno 2014).
between the MgII h and k lines, at 280.00 nm. The long-dashed curve in the top panels shows the height at which curves in the bottom panels correspond to the locations indicated with the vertical lines in the top panels for the respective line style. The long-dashed curve in the top panels shows the height at which $\tau = 1$ for the Mg II k line center. The dashed–double-dotted curve in the same panels shows the height at which $\tau = 1$ in the wings between the Mg II h and k lines, at 280.00 nm.

2.1. Atomic Model

In order to study the formation of the Mg II h and k lines (280.35 and 279.64 nm, respectively), we used an atomic model with three Mg II terms (five levels) and the ground level of Mg III. This atomic model is the one used in del Pino Alemán et al. (2020). The Mg II terms include the ground term, with the single $^2S_{1/2}$ level, and the first and third excited terms with the $^2P_{1/2}$ and $^2P_{3/2}$ levels and the $^2D_{3/2}$ and $^2D_{5/2}$ levels, respectively. The two excited terms in the model are radiatively connected by the $s_p$ (279.16 nm) and $s_c + s_v$ (279.88 nm) subordinate transitions. The subordinate triplet can be modeled with the complete frequency redistribution (CRD) approximation (Pereira et al. 2015).

2.2. Atmospheric Model

We model the emergent polarization profiles in a 2.5D rMHD simulation by Martínez-Sykora et al. (2020), carried out with the Bifrost code (Gudiksen et al. 2011). This model atmosphere includes ion–neutral interaction effects (i.e., ambipolar diffusion; Braginskii 1965) and nonequilibrium hydrogen and helium ionization (Leenaarts et al. 2011; Golding et al. 2014, 2016).

The simulation consists of 70 snapshots covering 700 s (10 s cadence). The computational box is 90 Mm wide, with a uniform horizontal resolution of 4 km, and 43 Mm of vertical extent, from 3 Mm below to 40 Mm above the visible solar surface. The vertical resolution is nonuniform, with a better resolution at the bottom of the model than higher up (about 12 km between $-0.5$ and 7 Mm and 70 km at the top of the simulation).

The simulation is representative of an active region plage with opposite magnetic polarities, with a mean magnetic field strength ($|B|$) of $\sim$200 G at the bottom of the photosphere and with a series of magnetic loops connecting the two regions. We do not calculate the emergent Stokes profiles for the whole simulation domain, but instead we limit our analysis to a 2° wide region around the negative polarity, which is dominated by acoustic shocks traveling into the upper layers of the atmosphere. We extract 1D vertical columns from the simulation, cutting just above the transition region. We show the plasma properties of this selected region in Figure 1.

3. Results: Theoretical Stokes Profiles

In this section we analyze the Stokes profiles obtained from the RT calculations. First, we show a selection of profiles calculated at the model resolution to understand how the thermal, dynamic, and magnetic stratifications affect the emergent Stokes profiles. Second, we create a synthetic observation that imitates the spatial and spectral resolution of the CLASP2 instrument and compare it with some available observations.

3.1. Stokes Profiles at the Model Resolution

After solving the RT problem in 84 columns in the rMHD model (14 columns in six snapshots of the series) we calculate the emergent Stokes profiles for a LOS with $\mu = 1$ (with
The asymmetries with $k_2v$ gradient in the region of formation with changing sign of the velocity is directed downward and is significantly different stratifications (see Figure 1), leading to Stokes profiles showing different spectral features.

Outside of the magnetic concentration, the intensity profiles show the characteristic double-peaked structure (the peaks are often denoted by $k_2v$ for the violet peak and $k_2r$ for the red peak with respect to the line center for the $k$ line, and $h_2v$ and $h_2r$ equivalently for the $h$ line) with a central depression (often denoted by $k_3$ and $h_3$ for the $k$ and $h$ lines, respectively) in both resonance lines. Moreover, the $k$ line intensity at the $k_2v$ and $k_2r$ peaks is always larger than that in the $h$ line peaks, $h_2v$ and $h_2r$. This behavior is usually found in quiet-Sun regions both in observations (Schmit et al. 2015) and in numerical calculations in semiempirical atmospheric models (del Pino Alemán et al. 2016, 2020).

The calculated emergent profiles show strong asymmetries due to the LOS velocity gradients. In the first snapshot we always find $k_2v > k_2r$ asymmetries (see the magenta dotted curve in Figure 2, where $k_2v$ is $\approx 7$ times larger than $k_2r$). In the corresponding column in the atmospheric model, at the deepest part of the formation region ($\approx 0.5$ Mm above the solar surface) we find an upward velocity of about 2.5 km s$^{-1}$, while at the top of the formation region the velocity is directed downward and is about $-5$ km s$^{-1}$, that is, there is a negative and relatively strong gradient in the region of formation with changing sign of the velocity. The asymmetries with $k_2v > k_2r$ seem to appear when there are negative gradients and downward plasma velocities along the line formation region. The opposite case, namely, $k_2v < k_2r$, can be found in other snapshots and it corresponds to positive gradients with upward velocity. These results are in agreement with the results of Leenaarts et al. (2013b) in a 3D rMHD model atmosphere.

In columns close to the center of the magnetic concentration, the intensity profiles show a significant enhancement of intensity in the far wings. Consequently, some of these intensity profiles resemble a more typical “absorption profile”, with $k_3$ and $h_3$ intensities smaller than those in the wings. An example of such a profile can be seen in the blue dashed curve in Figure 2. The double $k_2v$ peak in this profile is due to the presence of two temperature enhancements at two different heights along the LOS with different associated Doppler shifts (see the dashed curve in Figure 1). The increased temperature in the lower parts of the atmosphere is responsible for the larger intensity in the far wings.

Regarding the fractional circular polarization $V/I$ (see right column in Figure 2), we find the expected four-lobed shape (Alsinà Balles et al. 2016; del Pino Alemán et al. 2016) in the columns outside of the magnetic concentration, with the outer lobes always showing larger amplitude than the inner lobes, indicative of a negative gradient in the longitudinal component of the magnetic field (i.e., decreasing with height). In columns within the magnetic field concentration we find larger polarization signals and more pronounced asymmetries with respect to the line center. Some profiles show more than four lobes (see, e.g., the blue profile in Figure 2), which correspond to the superposition of different Doppler components (as explained above for the intensity profile corresponding to the same column in the model).

Regarding the profiles of fractional linear polarization $Q/I$ and $U/I$, their amplitudes are comparatively small in the region outside the magnetic field concentration ($<1\%$) and even smaller inside it ($<0.1\%$) for this LOS with $\mu = 1$ (disk-center observation). To better understand what the source of this linear polarization is$^4$ we have performed four numerical

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$^4$ We remind the reader that for an axially symmetric plane-parallel model atmosphere the only possible source of linear polarization in the emergent radiation for an LOS with $\mu = 1$ is the breaking of the axial symmetry due to the horizontal component of the magnetic field or of the macroscopic velocity.

Figure 2. Emergent intensity $I$ (left column) and fractional circular polarization $V/I$ (right column) for the four columns indicated in the top row in Figure 1 (indicated by the style of the line). The bottom row shows only the spectral region around the $k$ line at 279.64 nm.
experiments: (1) using the magnetic field and the velocity of the model, (2) using the magnetic field of the model, but neglecting the horizontal component of the velocity, (3) using the velocity of the model, but neglecting the magnetic field, and (4) neglecting both the magnetic field and the horizontal component of the velocity. The results are shown in Figure 3. As expected, the axially symmetric case (4) results in no fractional linear polarization. Comparing cases (2) and (3), we can see that the horizontal velocity is the main source of scattering linear polarization (for a detailed description of the generation and transfer of scattering polarization in the presence of horizontal velocity gradients, see Jaume Bestard et al. 2021). By comparing cases (1) and (3), we can see that the magnetic field mainly depolarizes this scattering linear polarization.

3.2. Stokes Profiles at CLASP2 Resolution

In order to compare the Stokes profiles of the radiation emerging from this model atmosphere with the observations obtained by the CLASP2 mission we have calculated a synthetic observation integrating the emergent radiation over 2″ and 60 s (similar to the angular resolution and the exposure time of the CLASP2 observations). To emulate a CLASP2 observation we apply both spectral and spatial degradation, convolving with a Gaussian of FWHM 0.11 Å and giving more prominence to the profiles located at the center of the selected region when we integrate over all the profiles (applying a Gaussian of FWHM 1″), respectively.

The resulting intensity profile shows a significant asymmetry between the two emission peaks, with a relatively deep central depression (k_{2v} > k_2, > k_3, see Figure 4). The dominant profiles are those from inside the magnetic concentration (they have the largest intensity and weight in the spatial convolution), and therefore this behavior was to be expected from the analysis in Section 3.1. Likewise, the fractional linear polarization signals are below ≈0.02%, also a consequence of the fact that the dominant profiles are those from inside the magnetic concentration. The fractional circular polarization shows a significant signal instead (≈2–3% for k and h, respectively). We can see in the fractional circular polarization profile (see bottom right panel of Figure 4) that the averaged profile still shows the asymmetries between the blue and red lobes that we found in the resolved profiles in the magnetic concentration (see Section 3.1).

Although the theoretical profiles of Figure 4 are more complex than the ones we usually find in plage observations (e.g., Ishikawa et al. 2021), we have found qualitatively similar intensity profiles in the IRIS database. A representative example, with a very deep central depression, asymmetric peaks (with k_{2v} > k_2 ), and an enhanced intensity in the far wings, is shown in Figure 5. This IRIS observation was carried out in coordination with the CLASP2.1 one. This intensity profile is found close to a plage region and at a magnetic concentration seen as a dark region; we know it is a magnetic concentration from the magnetogram from the same day provided by the Helioseismic and Magnetic Imager on the Solar Dynamics Observatory (SDO/HMI; Scherrer et al. 2012; Hoeksema et al. 2014). Likewise, we know that the presence of strong asymmetries in the profiles is indicative of strong gradients in the LOS velocity (Leenaarts et al. 2013b, and this work). It thus seems that the profile in Figure 5 could correspond to a region in the solar atmosphere with physical conditions akin to those found in the plage simulation.
4. Results: Suitability of the Weak-field Approximation

Recently Ishikawa et al. (2021) applied the WFA to the Stokes $I$ and $V$ profiles of the Mg II h and k lines observed by CLASP2 in order to infer the longitudinal component of the magnetic field ($B_{\text{LOS}}$) in the chromosphere of an active region plage. The validity of this approximation when applied to the Mg II resonant doublet was demonstrated with radiative transfer calculations with constant and stratified magnetic fields in 1D semiempirical models of the solar atmosphere. However, these semiempirical models are relatively smooth in their stratification of the physical parameters (temperature, density, and microturbulent velocity) and lack macroscopic velocities. In

Figure 4. Profiles of intensity $I$ (top left), fractional linear polarization $Q/I$ (top right) and $U/I$ (bottom left), and fractional circular polarization $V/I$ (bottom right) for a synthetic observation for an LOS with $\mu = 1$ emulating the spatial resolution ($2''$) and exposure time (60 s) of the CLASP2 observation.

Figure 5. Example of an IRIS observation near a magnetic concentration in a plage region. The left panel shows the slit-jaw image at 279.64 nm, and the white dot indicates the position of the profile shown in the right panel. The observation was performed on 2021 October 8 coordinated with the CLASP2.1 observations.
In this section we investigate the validity of the WFA to infer $B_{\text{LOS}}$ by applying it to a synthetic observation (Section 3.2) resulting from radiative transfer calculations in the time-dependent rMHD model described in Section 2.2, which has a complex stratification of the physical parameters and strong macroscopic velocities with gradients. $B_{\text{LOS}}$ inferred from the WFA can then be directly compared with the magnetic field in the rMHD model.

### 4.1. The Weak-field Approximation

The WFA (Landi Degl’Innocenti & Landolfi 2004) provides an analytical solution to the radiative transfer equations when some fundamental assumptions are satisfied. The first assumption is that the magnetic field strength must be weak enough to guarantee that the Zeeman splitting ($\Delta \lambda_B$) is significantly smaller than the Doppler width of the line ($\Delta \lambda_D$), i.e.,

$$g_{\text{eff}} \frac{\Delta \lambda_B}{\Delta \lambda_D} \ll 1,$$

with $g_{\text{eff}}$ the effective Landé factor of the line (1.30 and 1.16 for the h and k lines, respectively), $\Delta \lambda_B$ is the Zeeman splitting in angstrom:

$$\Delta \lambda_B = 4.6686 \times 10^{-13} B \lambda_0,$$

where $B$ is the magnetic field strength in gauss and $\lambda_0$ is the wavelength of the line in angstrom, and with the Doppler width

$$\Delta \lambda_D = \frac{\lambda_0}{c} \sqrt{\frac{2kT}{m}},$$

where $c$ is the speed of light, $k$ is the Boltzmann constant, $T$ is the plasma temperature, and $m$ is the mass of the atom.

The second assumption is that the longitudinal component of the magnetic field must be constant in the formation region of the spectral line. Then the Stokes $V$ profile is proportional to the longitudinal component of the magnetic field ($B_{\text{LOS}} = B \cos \theta_B$, with $\theta_B$ the angle between the field inclination and the LOS) and the first derivative of the intensity profile,

$$V = -4.6686 \times 10^{-13} g_{\text{eff}} \lambda_0 B_{\text{LOS}} \frac{\partial I}{\partial \lambda}. $$

### 4.2. WFA Suitability

The spatial extent of the Mg II h and k formation region makes fitting the whole circular polarization profile with the WFA virtually impossible, as $B_{\text{LOS}}$ changes significantly in the region of formation. Consequently, it is necessary to independently fit the inner and outer lobes of these lines in order to obtain a reliable inferred $B_{\text{LOS}}$ at the formation heights corresponding to such spectral regions (Ishikawa et al. 2021). Due to the strong asymmetries present in the profiles of circular polarization $V$ calculated in the rMHD model (see bottom right panel of Figure 4, and compare the red and blue outer lobes), fitting both of them together turns out to also be problematic and we have found that it is impossible to retrieve a reliable $B_{\text{LOS}}$ from such a simultaneous fit. For this reason, we decided to apply the WFA independently for the blue and red outer lobes, a decision that can be physically justified as will be shown below. In Figure 6 we show the application of the WFA to the circular polarization profile obtained in Section 3.2 following this fitting strategy. Table 1 includes the inferred values for $B_{\text{LOS}}$ using the different spectral ranges of these lines.

The green curve in Figure 6 shows the best fit between the circular polarization profile and the first derivative of the intensity when applied to the whole spectral range. It is clear that the circular polarization profile and the first derivative of the intensity are not proportional over the whole range, which is indicative of the stratification of $B_{\text{LOS}}$ along the region of formation of the line. However, when distinguishing between inner lobes, blue outer lobe, and red outer lobe, we can find a proportionality constant between the circular polarization profile and the first derivative of the intensity, thus obtaining three different values for $B_{\text{LOS}}$.

In order to understand the meaning of these multiple inferred $B_{\text{LOS}}$ values, we compare them with the longitudinal magnetic

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**Table 1**

| Line | Full | Core | Blue wing | Red wing |
|------|------|------|-----------|----------|
| k    | 312  | 175  | 542       | 373      |
| h    | 338  | 177  | 643       | 367      |
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Figure 7. Normalized average contribution function to the profile of circular polarization V in the rMHD model used in our RT calculations for the Mg II h line, for each frequency (bottom axis) and height (left axis). The black curve shows the stratification (left axis) of the average longitudinal magnetic field (top axis) over all the columns selected from the rMHD model. The orange, red, blue, and green dots show the values inferred for the longitudinal magnetic field by applying the WFA to the inner lobes, to the red outer lobe, to the blue outer lobe, and to the whole profile, respectively.

field found in the atmospheric model. To this end, we have taken the average of $B_{\text{LOS}}$ over the same pixels whose emergent Stokes profiles are included in the “observed” profile (see Section 3.2). In addition, we have calculated the contribution function to the profiles of circular polarization $V$ for each of those pixels, and took the same average. In Figure 7 we show both averages for the contribution function (for the Mg II h line, the figure for the k line is almost identical and thus it is not included) and the $B_{\text{LOS}}$ stratification, with colored dots marking $B_{\text{LOS}}$ inferred from the WFA from Figure 6. The contribution function gives us an idea of how each layer in the model atmosphere (left axis in the figure) contributes to the circular polarization profile at each wavelength (bottom axis). Together with the stratification of $B_{\text{LOS}}$ (top axis), we can thus get an idea of the height in the model atmosphere to which the inferred $B_{\text{LOS}}$ corresponds.

From the fit to the inner lobes (orange curve and dot in Figures 6 and 7, respectively) corresponding to $B_{\text{LOS}} = 177$ G, we can find this value at height $\approx 1.1$ Mm in the model atmosphere. From the contribution function, we see that the main contribution to the inner lobes indeed mainly comes from $\sim 1$–1.5 Mm. Regarding the fit to the blue (blue curve and dot) and red (red curve and dot) lobes, corresponding to $B_{\text{LOS}} = 643$ and 367 G, respectively, we can find these magnetic fields at heights $\sim 0$ and 0.4 Mm, respectively. From the contribution function we can indeed see that the main contribution to the positive blue lobe (strong blue region between 280.31 and 280.33 nm in the contribution function) is found around $\sim 0.2$ Mm, while the main contribution to the negative red lobe (strong red region between 280.37 and 280.38 nm in the contribution function) is found around $\sim 0.5$–0.8 Mm. Finally, the fit to the whole profile (green curve and dot) gives us $B_{\text{LOS}} = 338$ G, which corresponds to a magnetic field in between the maximum and minimum inferred for the different parts of the profile.

This experiment thus demonstrates that the WFA applied to fit different parts of the profile is able to retrieve $B_{\text{LOS}}$ values that correspond to the magnetic fields actually found at different heights in the model atmosphere. The velocity gradients found in the model introduce a relative shift of $\sim 400$ km between the formation heights of the outer lobes, and lead to a relatively complex contribution function (compare with Figure S6 in Ishikawa et al. 2021). This complexity is such that we can find opposite contributions to the circular polarization profiles in several wavelength ranges. These multiple contributions are the reason why the fit to the inner lobes in Figure 6 (orange curve) does not really reach the local maxima of those lobes, or why the inferred $B_{\text{LOS}}$ for the outer lobes is a bit lower in height than the actual contribution of the correct sign (blue and red colors in the contribution function for the blue and red outer lobes, respectively).

It is clear, however, that we do not have access to this information (contribution function) when working with actual observations. Therefore, without additional information, we cannot really determine to which region of the atmosphere the different $B_{\text{LOS}}$ correspond, beyond general descriptions such as mid to upper chromosphere (inner lobes) or lower to mid chromosphere (outer lobes). Moreover, the addition of photon noise will of course decrease the accuracy of the inferred $B_{\text{LOS}}$.

Nevertheless, the WFA is not only a quick and easy tool to apply to infer $B_{\text{LOS}}$ from the circular polarization profiles of Mg II h and k lines, but the inference it provides is representative of the actual magnetic field that produced such polarization. Moreover, the presence of strong velocity gradients that complicate the formation of the line not only does not impede the application of the WFA, but it can give access to $B_{\text{LOS}}$ in additional layers of the solar atmosphere (although it does not give information about where in the atmosphere).

5. Conclusions

In this work we have studied the formation of the polarized spectrum of the Mg II h and k lines in an rMHD model of a solar plage. To this end, we have performed polarized 1.5D RT calculations in a region around a magnetic concentration in a 2.5D rMHD simulation representative of a solar plage and analyzed the emergent Stokes profiles. These calculations take into account PRD effects as well as $J$-state interference between the upper levels of the Mg II h and k transitions. We have combined the emergent Stokes profiles to generate a synthetic observation mimicking the resolution of the CLASP2 observations (2″ of angular resolution and 156 s of exposure).

The selected region of the rMHD simulation shows strong gradients in the vertical (also the LOS) velocity, which results in Stokes profiles with significant asymmetries, confirming previous results in the literature (Leenaarts et al. 2013b). Even though we do not consider horizontal radiation transfer, the horizontal component of the velocity is one of the main contributors to the breaking of axial symmetry (see Jaume Bestard et al. 2021 for a study on the Ca I line at 4227 Å). The linear polarization due to this lack of axial symmetry in the
LOS to the disk center, however, is severely depolarized via the Hanle effect by the strong magnetic fields in this plage model.

Most of the intensity profiles emerging from the considered magnetic concentration region, as well as in the synthetic observation, show an asymmetry with \( k_2 > k_1 \) and \( k_1 \) below the intensity wings between the two lines of the doublet (likewise for the h line). Profiles with these properties are not typically found in observations. However, we have found an IRIS observation qualitatively similar to the intensity profile in our synthetic observation, corresponding to a magnetic concentration in a plage region. We thus expect that the physical conditions of the solar atmosphere corresponding to such an observation can be as complex as those found in the rMHD atmospheric model.

For our synthetic observation the profiles of fractional linear polarization \( Q/I \) and \( U/I \) show signals below \( \sim 0.02\% \). These relatively small signals would be of limited diagnostic potential for the magnetic field especially in observations affected by photon noise. However, the profile of fractional circular polarization \( V/I \) shows a remarkable signal above \( 2\% \) and thus can provide information on the longitudinal component of the magnetic field \( B_{\text{LOS}} \).

The main objective of this study has been to test the applicability of the WFA approximation to infer \( B_{\text{LOS}} \). The WFA approximation had been deemed suitable based on RT investigations in static 1D semiempirical models of the solar atmosphere with a constant or relatively smooth magnetic field stratification. However, it was not clear how the reliability of the inference could be affected by the strong velocity and magnetic field gradients typical of the solar atmosphere. We could not fit the circular polarization profile of our synthetic observation with a single \( B_{\text{LOS}} \), and not even with two different values for the inner and outer lobes, as in previous studies. By studying the contribution function to the circular polarization we have found that the velocity gradients are responsible for this impossibility. In fact, the formation region of the outer lobes of the circular polarization is shifted by about 400 km between them, and thus they map \( B_{\text{LOS}} \) in different regions in the model. By fitting individually each of the outer lobes we have been able to infer \( B_{\text{LOS}} \) in three different regions in the model atmosphere, corresponding to those regions that contribute the most to the circular polarization profile. Therefore, the fit to the inner lobes gave \( B_{\text{LOS}} \) in the mid–upper chromosphere, the fit to the red outer lobe gave \( B_{\text{LOS}} \) in the lower–mid chromosphere, and the fit to the blue outer lobe gave \( B_{\text{LOS}} \) in the photosphere.

Previous studies have shown that \( B_{\text{LOS}} \) inferred for the outer lobes of the circular polarization profile by applying the WFA is underestimated by about \( \sim 13\% \) due to PRD effects (del Pino Alemán et al. 2016; Centeno et al. 2022). However, this error is considerably smaller than the variation of the magnetic field in the formation region of the outer lobes (see Figure 7), and our conclusions about the suitability of the WFA remain valid.

Consequently, not only can the WFA be applied to the circular polarization profiles of the Mg II h and k lines, even in the presence of strong gradients in the underlying solar atmosphere, but these gradients can give us access to additional information about \( B_{\text{LOS}} \) in different layers within the atmosphere. However, the WFA is of course not enough to determine where in the atmosphere the inferred \( B_{\text{LOS}} \) is located, and alternative methods (e.g., inversions) need to be applied in order to get information about the formation height of the different parts of the Stokes profiles. Moreover, it is clear that photon noise in the circular polarization (not considered in this study because it is not relevant for our conclusions) will reduce the accuracy in the inference with respect to what is shown in this paper.

Due to the significant computational cost of generating a synthetic observation such as the one presented in Section 3.2, in this work we have focused on a single region (2 arcsec) of the rMHD simulation. Nevertheless, we have verified that the conclusions in Section 4.2 are also applicable to the individual 1.5D profiles, and therefore we can be confident of their validity not being limited to the studied region of this rMHD model. However, it can be interesting to extend this study to other rMHD simulations in the future in order to confirm the generality of our conclusions.

The results of this study confirm the validity of the methodology in Ishikawa et al. (2021) with regard to the Mg II lines, which showed the determination of \( B_{\text{LOS}} \) at several heights in the extended atmosphere of a solar plage. Moreover, they confirm how useful regular spectropolarimetric observations in the spectral region around the Mg II h and k lines could be for the magnetic diagnostic of the solar chromosphere, and in particular of the circular polarization profile, which gives us quick and relatively simple access to \( B_{\text{LOS}} \) via the WFA.

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**References**

Aalsina Ballester, E., Belluzzi, L., & Trujillo Bueno, J. 2016, ApJL, 831, L15
Belluzzi, L., & Trujillo Bueno, J. 2012, ApJL, 750, L11
Belluzzi, L., & Trujillo Bueno, J. 2014, A&A, 564, A16
Bohlin, J. D., Frost, K. J., Burr, P. T., Guha, A. K., & Withbroe, G. L. 1980, SoPh, 65, 5
Braginskii, S. I. 1965, RvPP, 1, 205
Calvert, J., Griner, D., Montenegro, J., et al. 1979, OptEn, 18, 287
Casini, R., del Pino Alemán, T., & Manso Sainz, R. 2017a, ApJ, 835, 114
Casini, R., del Pino Alemán, T., & Manso Sainz, R. 2017b, ApJ, 848, 99
Casini, R., Landi Degl’Innocenti, M., Manso Sainz, R., Landi Degl’Innocenti, E., & Landolfi, M. 2014, ApJ, 791, 94
Centeno, R., Rempel, M., Casini, R., & del Pino Alemán, T. 2022, ApJ, 936, 115
De Pontieu, B., Title, A., & Carlsson, M. 2014, Sci, 346, 315
Del Pino Alemán, T., Casini, R., & Manso Sainz, R. 2016, ApJL, 830, L24
Del Pino Alemán, T., Trujillo Bueno, J., Casini, R., & Manso Sainz, R. 2020, ApJ, 891, 91
Golding, T. P., Carlsson, M., & Leenaarts, J. 2014, ApJ, 784, 30
Golding, T. P., Leenaarts, J., & Carlsson, M. 2016, ApJ, 817, 125
Gudiksen, B. V., Carlsson, M., Hansteen, V. H., et al. 2011, A&A, 531, A154
Hanze, W., & Stenflo, J. O. 1987, SoPh, 111, 243
Hoeksema, J. T., Liu, Y., Hayashi, K., et al. 2014, SoPh, 289, 3483
Ishikawa, R., Bueno, J. T., del Pino Alemán, T., et al. 2021, SciA, 7, eabe8406
Jaume Bestard, J., Trujillo Bueno, J., Štepán, J., & del Pino Alemán, T. 2021, ApJ, 909, 183
Kerr, G. S., Allred, J. C., & Carlsson, M. 2019a, ApJ, 883, 57
Kerr, G. S., Carlsson, M., & Allred, J. C. 2019b, ApJ, 885, 119
Landi Degl’Innocenti, E., & Landolfi, M. 2004, Polarization in Spectral Lines, Vol. 307 (Dordrecht: Springer)
Leenaarts, J., Carlsson, M., Hansteen, V., & Gudiksen, B. V. 2011, A&A, 530, A124
Leenaarts, J., Pereira, T. M. D., Carlsson, M., Uitenbroek, H., & De Pontieu, B. 2013a, ApJ, 772, 89
Leenaarts, J., Pereira, T. M. D., Carlsson, M., Uitenbroek, H., & De Pontieu, B. 2013b, ApJ, 772, 90
Mano Sainz, R., del Pino Alemán, T., Casini, R., & McIntosh, S. 2019, ApJL, 883, L30
Martínez-Sykora, J., Leenaarts, J., De Pontieu, B., et al. 2020, ApJ, 889, 95
Mihalas, D. 1978, Stellar Atmospheres (San Francisco, CA: WH Freeman)
Milkey, R. W., & Mihalas, D. 1974, ApJ, 192, 769
Narukage, N., McKenzie, D. E., Ishikawa, R., et al. 2016, Proc. SPIE, 9905, 990508
Pereira, T. M. D., Carlsson, M., Pontieu, B. D., & Hansteen, V. 2015, ApJ, 806, 14
Priest, E. 2014, Magnetohydrodynamics of the Sun (Cambridge: Cambridge Univ. Press)
Sampoorna, M., Nagendra, K. N., & Stenflo, J. O. 2017, ApJ, 844, 97
Scherrer, P. H., Schou, J., Bush, R. I., et al. 2012, SoPh, 275, 207
Schmit, D., Bryans, P., De Pontieu, B., et al. 2015, ApJ, 811, 127
Štěpán, J., & Bueno, J. T. 2013, A&A, 557, A143
Sukhorukov, A. V., & Leenaarts, J. 2017, A&A, 597, A46
Trujillo Bueno, J., & del Pino Alemán, T. 2022, ARA&A, 60, 415
Trujillo Bueno, J., Landi Degl’Innocenti, E., & Belluzzi, L. 2017, SSRv, 210, 183
Uitenbroek, H. 1997, SoPh, 172, 109
Woodgate, B. E., Tandberg-Hanssen, E. A., Bruner, E. C., et al. 1980, SoPh, 65, 73