Experimental realization of phonon demultiplexing in three-dimensions

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ABSTRACT
Phononic metamaterials enabled the realization of many acoustic components analogous to their electronic counterparts, such as transistors, logic gates, and calculators. A key component among these is the demultiplexer, a device that receives multiple signals and sorts them based on their frequencies into separate channels. Previous experimental realizations of acoustic and elastic multiplexers have employed plates with pillars or holes to demultiplex frequencies. However, existing realizations are confined to two dimensions, which can limit potential acoustic or elastic circuit design. Here, we show an experimental realization of a three-dimensional, four channel phononic demultiplexer. Our design methodology is based on bundles of pass-bands within a large bandgap that can easily be tuned for multi-channel frequency demultiplexing. The proposed design can be utilized in acoustic and elastic information processing, nondestructive evaluation, and communication applications, among others.

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Phononic crystals and acoustic metamaterials consist of periodic arrangements of basic building blocks that repeat in space. These materials have the ability to control waves in an unprecedented manner, at different length and frequency scales. One of the unique properties of these materials is their ability to support forbidden frequency bands (i.e., bandgaps) in their dispersion spectrum. Within a bandgap, waves cannot propagate and are reflected toward the source. The main mechanisms for creating these forbidden bands within the frequency spectrum are either destructive interference (e.g., in Bragg scattering bandgaps) or local resonance. When a bandgap is open due to Bragg scattering, the wavelength of the affected waves is usually at the same order of the spacing between the unit cells (i.e., lattice spatial periodicity).1,2 In contrast, when a bandgap is open due to resonances, the wavelength of the attenuated waves can be independent of the lattice spacing.3 Such resonances induce properties that might not exist in conventional materials, like negative effective mass or stiffness.4–6 Phononic crystals and metamaterials with such exotic properties have been utilized for many applications such as vibration and sound insulation,7 seismic wave protection,9,10 wave guiding,11,12 and frequency filtering.13,14

Phononic crystals and metamaterials have been proposed as platforms to enable mechanical information processing. Potential applications range from thermal computing16–18 (at small scales) to ultrasound and acoustic based computing (at larger scales).19,20 Current realizations of fundamental phonon computing elements such as acoustic switches,21 rectifiers,22,23 diodes,24–26 transistors,27,28 memory,11 and lasers33,34 have been inspired by their electronic counterparts. Among such devices, demultiplexers are combinational logic devices that take a single input at one end and route it to one of the several output channels [Fig. 1(a)]. There exist multiple theoretical proposals for realizing phonon demultiplexers for both acoustic13,34,35 and elastic waves36–46 with few experimental demonstrations.30,47,48 The main working principle for most of these designs is based on embedded cylinders,11,36,37,49 holes,50 or pillars51 in a host plate. These realizations constrain demultiplexing phonons to two dimensions. A device that can demultiplex phonons in three dimensions for all wave polarization remains elusive. In this paper, we numerically design and experimentally characterize a 3D phonon demultiplexer for elastic waves [Fig. 1(b)].

To realize our demultiplexer, we design a cubic unit cell that has two important characteristics: (1) a wide bandgap to filter out...
undesirable frequencies and (2) a bundle of pass bands inside the large bandgap to allow only the targeted frequencies to pass. The unit cell is composed of eight masses, one at each of the unit cell’s corners, connected by 12 beams [Fig. 2(a)].

To verify our design hypothesis, we first consider an infinite unit cell model, where one single unit cell is assumed to repeat in space in all directions. We analyze the unit cell using Bloch periodic boundary conditions. The dispersion curves of the unit cell, correlating wavenumber with frequency, are calculated using the wave equations for heterogeneous media within an infinite medium. We use the finite element method to solve the elastic wave equations (COMSOL 5.4). The solution is the wavefunction $u(x, \kappa; t) = \tilde{u}(x) \exp(i(k_x x - \omega t))$, where $\tilde{u}$ is the Bloch displacement vector, $x$ is the position vector, $\kappa$ is the wavenumber, $\omega$ is the frequency, and $t$ is the time. The resulting dispersion curves are normalized by the unit cell size and the longitudinal speed of sound in the medium, $\Omega = \omega / c_x$. The dispersion non-dimensionalization comes at no loss of generality as it is first calculated with all the considered material parameters. The dispersion plot shows a significant bandgap [shaded gray region in Fig. 2(b)] with a relative width of $\approx 124\%$. The relative width of the bandgap is calculated as the absolute width of the bandgap divided by its central frequency. Within the bandgap region, there exist two pass bands with a central frequency of $\Omega = 0.29$ and 0.53, which we engineer to work as the transmission bands for our demultiplexer.

To better explain the behavior of the proposed design, we visualize the unit cell’s vibrational mode shapes by superimposing the displacement profiles as a heat map over its geometry for eight different frequencies [Fig. 2(c)]. The first two mode shapes ($\Omega_2 = 0.08$ and 0.1) resemble the first vibrational modes of the beams connecting the corner masses. The third and fourth modes ($\Omega_4 = 0.15$ and 0.17) show the mixed resonance modes of the corner masses along with the first vibrational modes of the connecting beams. All four modes exist below the bandgap. The fifth mode shape, which exists in the first passband ($\Omega_5 = 0.28$), shows the second vibrational mode of the connecting beams. The third vibrational mode of the unit cell beams manifests itself within the second passband ($\Omega_7 = 0.52$ and 0.55). At the edge of the bandgap ($\Omega_8 = 0.74$), the connecting beams vibrate in their fourth mode shape. The masses work as pivots or fixation points for the connecting slender beams, which behave as fixed-fixed beams with well-defined vibrational mode shapes. We note the existence of a very low frequency branch(es) along the path $\Gamma - X$ and $X - M$, due to the lack of the diagonal coupling between the corner masses. In addition, the simple geometry of the unit cell causes many of the vibrational mode shapes to be degenerate. Based on this simple design concept, the unit cell can be considered as a simple mass spring model with a large bandgap with embedded bands of transmission. By changing the diameter of the corner block, we can change the position of the bandgap and its width. Alternatively, by scaling the unit cell length along the $a$ direction, we can shift the position of the bandgap along with its embedded pass bands within the frequency spectrum. An advantage of scaling the entire unit cell, while keeping all aspect ratios the same, is preserving all the dispersion characteristics of the unit cell (e.g., group velocities) without alteration. This preservation can help in maintaining consistency in the performance of the different channels, such as the mode shapes and wave polarization.

The demultiplexer is constructed by designing four channels out of the same unit cell, but with four different lattice constants. All four
channels are connected at one end (i.e., the base of the demultiplexer). The excitation takes place at the base with multiple frequencies that get sorted into the four channels. To correctly confirm the behavior of the scaled unit cells, we calculate the dispersion curves for four different lattice constants \( a = 30, 36, 42, \) and \( 48 \) mm [Figs. 3(a), 3(c), 3(e), and 3(g)]. The dispersion curves for these four unit cells are calculated based on 1D Bloch periodicity (only along the \( k_x \) direction). Basing the analysis on 1D periodicity, as opposed to 3D periodicity, gives rise to extra modes along the free boundaries with no periodicity. These boundary modes manifest themselves as added lines in the dispersion curves. A clear difference between the 1D and 3D periodic dispersion curves can be seen, for example, by comparing the number of branches below the first bandgap in Figs. 2(b) and 3(a). A detailed comparison between 1D, 2D, and 3D periodicity is presented in the supplementary material. The existence of multiple flat or quasi-flat lines is mainly due to the added standing modes and does not affect the transmission signal. This can be seen in the amplitude of the transmission within the narrow pass bands in comparison to the transmission in the large pass bands at higher frequencies [Figs. 3(b), 3(d), 3(f), and 3(h)]. The predicted bandgap frequencies using the infinite unit cell model are shaded in gray in all panels of Fig. 3. The results of both the finite and infinite models are in very good agreement. Within the band gaps, shown as the gray shaded regions in Fig. 3, the amplitude of the transmitted wave is negligible motion.

The excitation takes place at the base with multiple frequencies that get sorted into the four channels. As more periodicity is incorporated in the model (i.e., along the \( x \) direction), less vibration modes become available at the free boundaries and the dispersion curves become identical to Fig. 2(b). Therefore, having a demultiplexer channel with more unit cells in all directions will result in less dispersion lines and wider band gaps. A variation in the presented design with input signals from all directions is presented in the supplementary material.

To experimentally validate our numerical simulations, we fabricate the demultiplexer through additive manufacturing (laser sintering) using polyamide (Young’s modulus \( E = 2.3 \) GPa and density \( \rho = 1.3\) g/cm\(^3\)) in the plate mode shapes) do not coincide with the operational frequencies of the channels. The channels are arranged in a \( 2 \times 2 \) grid separated by 30 mm. A harmonic excitation is applied at the bottom surface of the baseplate. We sweep the excitation frequency between 1 and 32 kHz and record the displacement at the end of each of the channels [Figs. 3(b), 3(d), 3(f), and 3(h)]. The predicted bandgap frequencies using the infinite unit cell model are shaded in gray in all panels of Fig. 3. The results of both the finite and infinite models are in very good agreement. Within the band gaps, shown as the gray shaded regions in Fig. 3, the amplitude of the transmitted wave is many orders of magnitude less than that of the passband frequencies. The fact that all channels are connected at the base does not affect the robustness of the individual channels’ performance. In addition, we also plot the logarithm of the full displacement fields as a heat map at the four operational frequencies of the demultiplexer (Fig. 4). The displacement field at each frequency shows a clear transmission of elastic phonons at targeted frequency, while the rest of the channels show negligible motion.

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at half the size would operate around twice the frequency (i.e., in the with no geometry alteration. For example, the same design fabricated fabrication and the material invariant nature of the design principle, recent progress in advanced manufacturing. Due to these advances in higher dimensional all-phononic circuits, taking advantage of the of the wave allows for phonon demultiplexing in three dimensions. The experimental measurements show clear evidence of phonon transmission of the signal in the designated pass bands in each channel. The complete bandgap allows for a wider operational bandwidth and ensures transmission of each signal to its designated channel. The complete bandgap of each pass band allows for a wider operational bandwidth and ensures transmission of each signal to its designated channel. The complete bandgap for all directions and polarization (in-plane, out of plane, and rotation) for all signals. In general, the measured signals at the end of each channel are in very good agreement with the numerical simulations. In particular, the size and position of the bandgaps seem to support our numerical predictions. More importantly, the measured vibrations between 10 and 20 kHz show a clear bandgap, as predicted by the numerical simulations in all channels, and demonstrate clear transmission of the signal in the designated pass bands in each channel. The experimental measurements show clear evidence of phonon demultiplexing based on frequency in the realized meta-device.

In this study, we design, analyze, and realize the first 3D phononic demultiplexer. Our design relies on defining relatively narrow pass bands within a wide bandgap. Designing the width of the passband allows for a wider operational bandwidth and ensures transmission of each signal to its designated channel. The complete bandgap for all directions and polarization (in-plane, out of plane, and rotation) of the wave allows for phonon demultiplexing in three dimensions. Multiplexing elastic and acoustic waves in 3D can enable the design of higher dimensional all-phononic circuits, taking advantage of the recent progress in advanced manufacturing. Due to these advances in fabrication and the material invariant nature of the design principle, our meta-device can be easily scaled to operate at desired frequencies with no geometry alteration. For example, the same design fabricated at half the size would operate around twice the frequency (i.e., in the ultrasound regime). Our demultiplexer has possible applications in imaging, communications, and phonon-based information processing.

See the supplementary material for detailed dispersion curves with different periodic boundary conditions and an alternative design of the multiplexer based on our unit cell.

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DATA AVAILABILITY

All the data supporting the findings in this study are available in this article and its supporting information. Further data and methods are available from the corresponding author upon reasonable request.

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