Tuning Spin-Orbit Torques Across the Phase Transition in VO$_2$/NiFe Heterostructure

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The emergence of spin-orbit torques as a promising approach to energy-efficient magnetic switching has generated large interest in material systems with easily and fully tunable spin-orbit torques. Here, current-induced spin-orbit torques in VO$_2$/NiFe heterostructures are investigated using spin-torque ferromagnetic resonance, where the VO$_2$ layer undergoes a prominent insulator-metal transition. A roughly twofold increase in the Gilbert damping parameter, $\alpha$, with temperature is attributed to the change in the VO$_2$/NiFe interface spin absorption across the VO$_2$ phase transition. More remarkably, a large modulation (±100%) and a sign change of the current-induced spin-orbit torque across the VO$_2$ phase transition suggest two competing spin-orbit torque generating mechanisms. The bulk spin Hall effect in metallic VO$_2$, corroborated by the first-principles calculation of the spin Hall conductivity $\sigma_{SM} = -10^4 \frac{\hbar}{e} \Omega^{-1} m^{-1}$, is verified as the main source of the spin-orbit torque in the metallic phase. The self-induced/anomalous torque in NiFe, with opposite sign and a similar magnitude to the bulk spin Hall effect in metallic VO$_2$, can be the other competing mechanism that dominates as temperature decreases. For applications, the strong tunability of the torque strength and direction opens a new route to tailor spin-orbit torques of materials that undergo phase transitions for new device functionalities.

1. Introduction

Long-term goals of spintronics are the generation and the utilization of spin currents for information processing and storage.[1-2] Compared to optical and electrical spin injection schemes,[3,4] the spin current generation via spin-orbit interaction has demonstrated efficient charge-to-spin conversion[5,6] and has received much interest not only in the fundamental understanding but also in particular for technological applications. Notably, magnetization switching via spin-orbit torques[7,8] offers a number of advantages over conventional spin-transfer torque switching and is actively being developed into new generation spintronics devices such as spin-orbit torque magnetoresistance random access memory.[9]

The main mechanisms behind these recent advances are the current-induced spin-orbit torques.[10,11] The torques can be realized in a number of different ferromagnet–nonmagnet systems, and efficient charge-to-spin conversion was observed not only in conventional metallic heterostructures but also in nonmagnetic metal bilayers,[12] semiconductor quantum wells,[13-15] and topological insulators.[16-18] So far various mechanisms for the observed spin-orbit torques have been identified; however, very often it has been challenging to identify the origin of the spin-orbit torques because different mechanisms contribute at the same time and compete with each other. Furthermore, varying layer thicknesses in order to disentangle bulk and interface effects poses difficulties as the growth
and interface properties change with varying thicknesses. For the bulk effects, the spin Hall effect of the nonmagnet has been regarded as one of the main contributions and the values can now also be calculated theoretically.\cite{6,8} Meanwhile, although the effect of spin-orbit coupling in the ferromagnet has been regarded as negligible so far, a recent experiment\cite{19} revealed that even a single ferromagnet can generate substantial self-induced torque with a defined sign. Moreover, it was shown that orbital Hall currents generated from the nonmagnetic layer can also contribute strongly to the torque.\cite{20}

The spin-orbit torque efficiency is a parameter that is usually set for a specific material and interface, and it cannot be modulated easily. While it has been recently shown that strain can be used to control the spin-orbit torque to some extent,\cite{21} a piezoelectric substrate is often required that complicates growth and optimization of thin films. In this respect, an interesting material is vanadium dioxide (VO$_2$), a transition metal oxide that undergoes a prominent insulator–metal transition with temperature. The hysteretic phase transition allows to deliberately switch between insulating and metallic states, which can then influence the current flow and thus spin-orbit effects. The change in the VO$_2$ orbital occupation\cite{22} across the structural phase transition leads to the large changes in electrical resistivity\cite{23} as well as optical,\cite{24} structural,\cite{25} and magnetic properties\cite{26–28} and is expected to affect the spin-orbit coupling directly.\cite{29} However, the effect of the VO$_2$ phase transition on current-induced spin-orbit torques in a VO$_2$/ferromagnet heterostructure, which is of key importance for the future functionalization, has not been investigated and therefore is the main focus of this study.

In this work, we investigate current-induced spin-orbit torques in a VO$_2$/NiFe heterostructure across the VO$_2$ insulator-metal phase transition with the emphasis on the functionalization. The sign and the magnitude of the generated spin-orbit torques are probed using the spin-torque ferromagnetic resonance (ST-FMR) technique, where we inspect resonance linewidths of the bilayer strips with an additional DC current through the strip. Due to the several orders of magnitude changes in the electrical resistivity of the VO$_2$ layer across the phase transition, the ratio of the applied charge currents in the VO$_2$ and the NiFe layers is thus controlled by changing temperature. In particular, we quantify the large variation including a sign change of spin-orbit torque in different VO$_2$ phases. The observed hysteretic, phase-dependent spin-orbit torques could be utilized for future device concepts.

2. ST-FMR Measurements Across Insulator–Metal Transition

First, several structural characterizations were performed to inspect the quality of the VO$_2$ films. Figure 1a shows an out-of-plane x-ray diffraction plot of the 70 nm thick VO$_2$ film deposited by reactive sputtering on Al$_2$O$_3$(1-102). The (110), (200), and (111) VO$_2$ peaks are visible, indicating the polycrystalline growth of the VO$_2$ film. In Figure 1b, a 1 µm $\times$ 1 µm atomic force microscopic image of the same film shows large structural domains of a few hundred nanometer sizes with a root-mean-square roughness of 6.3 nm. Figure 1c displays the temperature dependence of four-probe van der Pauw resistance of the VO$_2$ film. d) SQUID M-H loops of the VO$_2$ (70 nm)/NiFe (5 nm) bilayer measured at 300 K.

Figure 1. Structural properties and insulator-metal transition of VO$_2$. a) Out-of-plane XRD scan of the 70 nm VO$_2$ film on the Al$_2$O$_3$(1-102) substrate. b) 1 µm $\times$ 1 µm atomic force micrograph and c) temperature dependence of four-probe van der Pauw resistance of the VO$_2$ film. d) SQUID M-H loops of the VO$_2$ (70 nm)/NiFe (5 nm) bilayer measured at 300 K.
dependence of van der Pauw resistance of the as-deposited VO_2 film, where an insulator–metal transition with temperature results in a resistance change of four orders of magnitude, as observed previously.[23] In order to characterize the current-induced spin-orbit torques of the VO_2 layers, a Ni_{81}Fe_{19} (5 nm)/MgO (2 nm)/Ta (3 nm) multilayer stack is sputter-deposited on top of the VO_2 (70 nm) film. M-H hysteresis loops of the resulting multilayer stack measured at 300 K are shown in Figure 1d. The magnetically soft NiFe layer is fully saturated by a 10 mT magnetic field to within 10% of the expected bulk saturation value of \( \approx 8.8 \times 10^5 \text{ A m}^{-1} \), with a coercivity less than 1 mT.

The VO_2/NiFe/MgO/Ta structure (Figure 2a) is patterned into a 10 \( \mu \text{m} \) wide strip and embedded into a coplanar-waveguide circuit, as seen in the measurement schematic in Figure 2b. Details of the patterning process can be found in the Supporting Information Section II. The temperature-dependent resistance of the patterned device stack is shown in Figure 2c. In the patterned strip, the insulator–metal transition becomes broader in temperature than in the unpatterned film (Figure 1c), which we account to edge defects created during the patterning process. ST-FMR field sweeps of the sample measured at different sample temperatures between 290 and 355 K are shown in Figure 2d. The sample temperatures were controlled using a Peltier element directly under the sample. The ST-FMR signal, \( V_{\text{mix}} \), which effectively measures the RF-current-rectified anisotropic magnetoresistance of the strip, is enhanced when the applied magnetic field and the RF current frequency matches the resonance condition for the NiFe moment precession. The obtained ST-FMR line shape can be represented as a superposition of symmetric and antisymmetric Lorentzian components using the equation[30,31]

\[
V_{\text{mix}} = S \frac{W^2}{(\mu_0 H - \mu_0 H_{\text{res}})^2 + W^2} + A \frac{W (\mu_0 H - \mu_0 H_{\text{res}})}{(\mu_0 H - \mu_0 H_{\text{res}})^2 + W^2} + V_{\text{const}} \quad (1)
\]

where \( S \) and \( A \) are the symmetric and the anti-symmetric coefficients, \( W \) is the resonance linewidth, \( \mu_0 \) is the vacuum permeability, \( H_{\text{res}} \) is the resonance field, and \( V_{\text{const}} \) is an offset voltage in the measurement. The symmetric component, \( S \), of \( V_{\text{mix}} \) is proportional to the damping-like torque generated by the spin current from the bulk VO_2 layer and the VO_2/NiFe interface, while the antisymmetric component, \( A \), is generated by the Oersted field produced by the RF excitation current as well as the field-like torque arising from the spin current. The RF frequency dependence of \( H_{\text{res}} \) and \( W \) can be seen in Figure S2 (Supporting Information). As the sample temperature increases, the VO_2 becomes more metallic and the amount...
of the RF current through the NiFe layer that produces the $V_{\text{mix}}$ signal decreases.

The relationship between the resonance linewidth $W$ and the driving frequency $f$ can be described by

$$W = W_0 + \frac{2\pi\alpha}{|\gamma|} f$$

where $W_0$ is the inhomogeneous broadening, $\gamma$ is the electronic gyromagnetic ratio of NiFe (where a value of 185 GHz T$^{-1}$ is used based on the electron Landé $g$-factor of 2.1$^{18}$) and $\alpha$ is the effective Gilbert damping constant of the bilayer. The temperature dependence of the effective Gilbert damping parameter $\alpha$, as shown in Figure 3, is obtained by performing the ST-FMR measurements at different temperatures. The values of $\alpha$ increased from $(0.035 \pm 0.010)$ at 290 K to $(0.06 \pm 0.01)$ at 355 K. The increase of $\alpha$ with temperature can be attributed to the combined effects of the increased magnon population in NiFe at higher temperatures and the enhanced spin current absorption$^{12}$ at the VO$_2$/NiFe interface as the VO$_2$ becomes metallic (spin pumping enhancement). The total device resistance during the same thermal cycle is also plotted in the same figure to directly compare the temperature-dependence of $\alpha$ and the VO$_2$ phase transition.

3. Temperature-Dependence of DC-Induced Spin-Orbit Torques

In this system, the next key step for functionalization is to quantify current-induced spin-orbit torques across the VO$_2$ phase transition. In order to examine this, we pass an additional DC current, $I_{\text{DC}}$, through the strip (as seen in the schematic in Figure 2b) and study how this additional stimulus affects the ST-FMR spectra, namely the linewidth $W$, at different temperatures. With the additional DC current, the current-induced spin-orbit torques generated in the VO$_2$ layer and the VO$_2$/NiFe interface exert damping-like torques on the precessing NiFe magnetization. Depending on the sign of the torque (which in turn depends on the directions of the current, $I_{\text{DC}}$, and the external magnetic field, $H_{\text{ext}}$), the linewidth $W$ broadens or narrows. This can be observed in Figure 4a, where the application of the 1 mA ($\sim$1 mA) DC bias broadens (narrows) the linewidth $W$, compared to the spectrum at 0 mA. The obtained changes in the linewidth, $\Delta W$, with our range of DC currents are a fraction of the original linewidth and comparable to the uncertainty in the linewidth estimation from the fitting according to the Equation (1). Therefore, the field sweep measurements are repeated between 20 and 50 times and the value of $W$ are obtained by averaging. The uncertainties in $W_{\text{avg}}$ are obtained by the statistical deviation of $W$,

$$\sigma_{W_{\text{avg}}} = \frac{\sum_{i=1}^{N}(W_i - W_{\text{avg}})}{N}$$

The Table 1 shows the values of $W_{\text{avg}}$, $\sigma_{W_{\text{avg}}}$, the number of field-sweeps and the average $R^2$ values for the measurements at 290 K.

The changes in the linewidth $W$ with the added DC current are shown in Figure 4b,c at 290 K and 355 K, respectively. (The ST-FMR spectra with DC currents at different temperatures can be seen in Figure S4, Supporting Information.) The change in the linewidth is linearly proportional to the magnitude of the DC bias, indicating that the generated spin current is also linearly proportional to the applied charge current.

Remarkably, we have observed a sign change of the torques across the phase transition of VO$_2$, suggesting competing origins of the spin-orbit torques. Figure 4d summarizes the DC-induced linewidth changes, $\Delta W/I_{\text{DC}}$, at different temperatures, as compared to the device resistance across the phase transition. At 290 K, the VO$_2$ layer resistance is several orders of magnitude higher than that of the NiFe layer, and most of the applied DC current flows through the NiFe layer. The lack of the DC current flowing through the VO$_2$ layer eliminates the bulk spin Hall effect in the VO$_2$ as the main origin of the large spin-orbit torque is observed at this temperature. The effect of the self-induced torque in NiFe, as observed in Ni,$^{19}$ can explain our observed sign of the signal. Additional interfacial effects, such as inverse spin galvanic effect prominent in many Rashba-like interfaces,$^{15,17,13}$ can also additionally contribute but these effects have been reported of not having a unique sign of the generated torques. Furthermore, as the interface between the VO$_2$ and the NiFe is present in both the low and high temperature phases, it is not clear that strongly different inverse spin galvanic effects can be expected as a function of temperature.

As the temperature increases, VO$_2$ undergoes an insulator-metal transition and more current flows through the VO$_2$ layer (The device resistance dependence of the $\Delta W/I_{\text{DC}}$ can be found in Figure S5, Supporting Information.). Therefore, this charge current can create spin currents in the VO$_2$ layer by the bulk spin Hall effect, which competes with the other contributions such as the self-induced torque from NiFe or the interfacial torque. As shown in Figure 4d, the observed total spin-orbit torque decreases in magnitude with an increase in the temperature from 290 K, goes through the sign change at $\approx 325$ K near the middle of the insulator–metal transition, then
increases again in magnitude to 355 K. The spin-orbit torque generated via the bulk spin Hall effect in the metallic VO$_2$ layer at 355 K is of the same sign as seen in V/CoFeB [34] and VO$_2$/YIG [32] (negative effective spin Hall angle).

### 4. First-Principles Calculation of Spin Hall Conductivity in Metallic VO$_2$ and Discussion

Taking into account all the above points, the large changes in the spin-orbit torque observed in our system can be interpreted by two competing mechanisms. One of the major changes brought forward by the insulator–metal transition is the electric current flowing within the VO$_2$ layer. In the metallic phase of the VO$_2$, this current in turn generates spin/orbital Hall current, which is injected into NiFe layer and thus exerts a torque. In order to estimate this effect quantitatively, we performed first-principles calculations of spin and orbital Hall conductivities of the metallic VO$_2$ in the rutile structure, as shown in Figure 5. In the figure, we show the spin Hall conductivity, $\sigma_{SH}$ (blue line), and the orbital Hall conductivity, $\sigma_{OH}$ (red line), as a function of the Fermi energy ($E_F$) with respect to the true Fermi energy ($E_{F, true}$), where $E_F$ is varied assuming that the potential is fixed to the potential for $E_{F, true}$. The result indicates that there are two peaks for $\sigma_{SH}$ near $E_{F, true} \approx 0$. On the other hand, a peak of $\sigma_{OH}$ is located at $\approx 0.3$ eV above $E_{F, true}$. The values for the spin and orbital Hall conductivities at the true Fermi energy are $\sigma_{SH} = -96$ (h/e) (Ω cm)$^{-1}$ and $\sigma_{OH} = +320$ (h/e) (Ω cm)$^{-1}$, respectively. More details of the calculation can be found in Supporting Information Section IV. Although the orbital Hall conductivity is larger than the spin Hall conductivity, its contribution to the torque is expected to be negligible. Here, since the orbital-to-spin conversion ratio in NiFe is expected to be <10%. We would like to point out that the sign of

Table 1. The average linewidths, errors, the number of field sweeps and the average $R^2$ values for the 290 K data.

| DC [mA] | $W_{avg,45^\circ}$ [mT] | $\sigma W_{avg,45^\circ}$ [mT] | N | Average $R^2$ | $W_{avg,-135^\circ}$ [mT] | $\sigma W_{avg,-135^\circ}$ [mT] | N | Average $R^2$ |
|---------|--------------------------|-----------------------------|---|-------------|--------------------------|-----------------------------|---|-------------|
| -0.5    | 25.2                     | 0.4                         | 48 | 0.94        | 27.9                     | 0.4                         | 49 | 0.96        |
| -0.25   | 27.1                     | 0.4                         | 49 | 0.95        | 27.5                     | 0.4                         | 49 | 0.95        |
| 0.01    | 27.6                     | 0.3                         | 50 | 0.96        | 26.9                     | 0.3                         | 50 | 0.97        |
| 0.25    | 28.1                     | 0.4                         | 50 | 0.95        | 25.3                     | 0.3                         | 50 | 0.95        |
| 0.5     | 30.2                     | 1.1                         | 50 | 0.96        | 24.9                     | 0.4                         | 50 | 0.95        |
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Figure 5. Spin and orbital Hall conductivity for the metallic VO2. The crystal structure is shown in upper left, where grey and red spheres represent V and O atoms, respectively. The spin Hall conductivity (σSH) and orbital Hall conductivity (σOH) are displayed as a function of the Fermi energy (EF) with respect to the true Fermi energy (Etrue,F), which are indicated by solid blue and red lines, respectively. The values at Etrue,F are σSH = −96 (h/e) (Ω cm)−1 and σOH = +320 (h/e) (Ω cm)−1, respectively.

computed spin Hall conductivity is consistent with the sign of the effective spin Hall angle measured in the experiment, which allows us to conclude that the spin Hall effect of the VO2 is one of the main mechanisms for the torque when VO2 is driven into the metallic phase. Meanwhile, there can be another contribution by the so-called self-induced torque/anomalous spin-orbit torque in the ferromagnetic layer itself. As predicted and experimentally observed previously, this can be interpreted as the transfer of spin angular momentum between spin-polarized charge currents and magnetization. While the spin Hall conductivity from this anomalous spin-orbit torque in NiFe itself was found to be large at ≈2300 (h/e) (Ω cm)−1, the value reduces to 10–100 (h/e) (Ω cm)−1 at an interface with a non-magnetic layer such as Cu and AlOx, due to the additional angular momentum loss to the lattice via spin-orbit coupling. The expected magnitude and the positive sign of the spin Hall conductivity explains well the observed behavior in our NiFe/VO2 bilayer system across the VO2 phase transition. At the VO2 insulating regime, the spin-orbit torque arises from the self-induced torque of the NiFe layer, while as the VO2 becomes more metallic across the phase transition, the bulk and the negative spin Hall effect from the VO2 dominates and reverses the spin-orbit torque direction.

Finally, there may be a contribution to the torque originating in the interfacial scattering, but we expect that the interfacial contribution does not change drastically across the insulator-metal transition since the strain induced by the structural phase transition is small (typically of ~1%).

We can now compare our results with the previous spin-pumping inverse spin Hall effect (SP-ISHE) measurements in VO2/YIG. In this system, the only source of the observed ISHE signal is the spin-to-charge conversion within the VO2. Therefore, there is no phase-dependent reversal of the signal with temperature, but only the broadening and the reduction of the signal due to the increased interface spin-transparency at the high temperature metallic phase, which is also observed in our case as an increase in the Gilbert damping parameter α (Figure 3). In VO2/YIG, the SP-ISHE signal is largely affected by the conductivity change of the VO2, which is observed as a sharp decrease in the signal at high temperature. In our system, the ST-FMR signal depends on the rectified AMR effect in NiFe, whose conductivity does not change significantly across the VO2 phase transition. This allows for the measurements of spin-orbit torques present at the VO2/ferromagnet interface directly across the VO2 phase transition.

As studied in depth using X-ray absorption spectroscopy, the change in the VO2 orbital occupation across the phase transition is likely to affect directly the current-induced spin-orbit torque generation mechanisms. The investigation of the orbital correlation and its effect in the spin-orbit torque at the VO2/ferromagnet interface is reserved for a future work.

5. Conclusions
We have measured the current-induced spin-orbit torques in the VO2/NiFe bilayer system using the spin-torque ferromagnetic resonance technique. A sign change of the damping-like spin-orbit torques with temperature is observed across the VO2 layer phase transition. The spin change and the modulation of the observed torques with temperature suggest coexistence of various competing mechanisms, mainly the bulk spin Hall effect in metallic VO2, corroborated by our first-principles calculation, and the self-induced torque in NiFe. While additional interfacial effects can play a role, we expect these not to change significantly across the transition, but additional measurements could be carried out to identify further possible contributions. For applications, the large (±100%) modulation, as well as the sign change of the spin-orbit torque enables full tunability of the torque to any desired value via device thermal history engineering, leading to potentially drastically different device architectures.

Supporting Information
Supporting Information is available from the Wiley Online Library or from the author.

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Conflict of Interest
The authors declare no conflict of interest.

Author Contributions
M.K., I.K.S., and D.-S.H. proposed and designed the experiments. P.S., P.N.L., and N.M.V. optimized, deposited, and characterized the VO₂ samples. J.C. deposited the magnetic stack. J.K. fabricated the devices. D.-S.H., J.K., and K.L. constructed the ST-FMR measurement system. J.K. performed the ST-FMR experiments and analyzed the experimental data with help from G.J., M.K., D.G., and Y.M. performed the first-principles spin Hall conductivity calculations. J.K. wrote the manuscript through multiple iterations by all authors.

Data Availability Statement
The data that support the findings of this study are available from the corresponding author upon reasonable request.

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