How Galactic Environment Affects the Dynamical State of Molecular Clouds and Their Star Formation Efficiency

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Abstract

We investigate how the dynamical state of molecular clouds relates to host galaxy environment and how this impacts the star formation efficiency (SFE) in the Milky Way and seven nearby galaxies. We compile measurements of molecular cloud and host galaxy properties, and determine mass-weighted mean cloud properties for entire galaxies and distinct subregions within. We find molecular clouds to be in ambient pressure-balanced virial equilibrium, where clouds in gas-rich, molecular-dominated, high-pressure regions are close to self-virialization, whereas clouds in gas-poor, atomic-dominated, low-pressure environments achieve a balance between their internal kinetic pressure and external pressure from the ambient medium. The SFE per free-fall time of molecular clouds is low, ~0.1%–1%, and shows systematic variations of 2 dex as a function of the virial parameter and host galaxy environment. The trend observed for clouds in low-pressure environments—as the solar neighborhood—is well matched by state-of-the-art turbulence-regulated models of star formation. However, these models substantially overpredict the low observed SFEs of clouds in high-pressure environments, which suggest the importance of additional physical parameters not yet considered by these models.

Key words: ISM: clouds – ISM: kinematics and dynamics – ISM: structure – galaxies: ISM – galaxies: star formation – stars: formation

Supporting material: machine-readable table

1. Introduction

Stars form in molecular clouds. For galaxies on the star formation main sequence (see reviews by Blanton & Moustakas 2009; Renzini & Peng 2015), the molecular gas mass ($M_{\text{mol}}$) and star formation rate (SFR) are tightly correlated (see reviews by Kennicutt & Evans 2012; Krumholz 2014). This tight correlation holds for entire galaxies (Kennicutt 1998; Young et al. 1995; Saintonge et al. 2011a) and down to kiloparsec-scale regions (Bigiel et al. 2011; Leroy et al. 2013b), below which differences in the evolutionary state of individual star-forming regions introduce significant scatter (Onodera et al. 2010; Schruba et al. 2010; Feldmann et al. 2011; Kruisjsten & Longmore 2014; Kreckel et al. 2018).

For main-sequence galaxies, the molecular gas depletion time, $\tau_{\text{dep}} = \Sigma_{\text{mol}}/\Sigma_{\text{SFR}}$, is of order 1–2 Gyr (Leroy et al. 2013b) and has experienced only modest evolution through cosmic times (Saintonge et al. 2013). This implies that star formation on galactic scales is highly inefficient, with only a few percent of a galaxy’s gas mass being converted to stars per free-fall time over the disk scale height (Krumholz et al. 2012). Importantly, $\tau_{\text{dep}}$ shows systematic second-order variations: longer $\tau_{\text{dep}}$ are found in massive, bulge-dominated spiral galaxies (Saintonge et al. 2011b; Shi et al. 2011), early-type galaxies (Wei et al. 2010; Davis et al. 2014), and (potentially) low-mass dwarf galaxies (Hunt et al. 2015; Amorín et al. 2016; Grossi et al. 2016; but see Filho et al. 2016), while shorter $\tau_{\text{dep}}$ are found in (many) galaxy centers (Leroy et al. 2013b) and gas-rich early-universe galaxies (Tacconi et al. 2013, 2018). Understanding what regulates the (in-)efficiency of star formation and results in the observed gas–SFR relationship, its normalization (i.e., $\tau_{\text{dep}}$), and variations thereof in different galactic environments is therefore a key task to understand galaxy evolution.

Disk equilibrium models try to explain a galaxy’s SFR by a dynamical balance of gravitational forces promoting star formation, and energy and momentum feedback by recently formed stars counteracting gravitational collapse (Toomre 1964; Ostriker et al. 2010; Hopkins et al. 2011; Kim et al. 2011; Romeo & Wiegert 2011; Faucher-Giguère et al. 2013; Agertz et al. 2015; Hayward & Hopkins 2017; Krumholz et al. 2017). In these models, the SFR self-regulates to produce stellar feedback just sufficient to keep the galaxy’s gas disk in vertical pressure and energy balance and marginally stable against radial instabilities. As the radial and vertical distributions of stars, gas, and dark matter in the galaxy vary, so does the SFR per unit gas mass needed to maintain equilibrium. This leads to different values of $\tau_{\text{dep}}$ in galaxy centers, outer disks, and dwarf galaxies (see above references).

Limitations of these models have been the dependence on phenomenological star formation prescriptions and a highly uncertain feedback efficiency. They have also tended to adopt a simplified modeling of the ISM structure relevant to gravitationally unstable (Romeo & Wiegert 2011; Agertz et al. 2015) and treat the cold, star-forming gas in a simple way. To date, the fraction of cold, molecular, star-forming gas has been represented either as a pressure-regulated (Ostriker et al. 2010; Kim et al. 2011) or shielding-regulated two-phase medium (Krumholz 2013), with little distinction between different physical states within the molecular gas. The first models that also consider the dynamical state (i.e., gravitational boundedness) of the cold, star-forming gas in a galactic context (Semenov et al. 2016; Krumholz et al. 2018) have recently been presented. However, a fully self-consistent theory of
galactic and cloud-scale properties with essentially no meaningful free parameters remains to be developed.

**Turbulent cloud models** attempt to predict the galaxy’s SFR from the star formation efficiency (SFE)\(^5\) of individual turbulent molecular clouds (Equation (8); Krumholz & McKee 2005; Hennebelle & Chabrier 2011; Padoan & Nordlund 2011; Federrath & Klessen 2012). These represent the smaller-scale complement to the disk equilibrium models. In these models, the mean density, gravitational boundedness, and Mach number play a central role as they define the cloud’s density structure, balance of kinetic and gravitational energy, and the mass in self-gravitating dense clumps where stars form. Star formation in these clouds progresses on a few dynamical timescales, typically parameterized by the gravitational free-fall time \((\tau_{ff} \propto \rho^{-0.5})\), though at a low efficiency per free-fall time, \(\epsilon_{ff} \approx 1\%\) (Krumholz & Tan 2007).

Observable properties of molecular clouds, such as their size \((R)\), velocity dispersion \((\sigma_v)\), and surface density \((\Sigma)\), offer a snapshot view of their dynamical state, which the models employ to predict the cloud’s SFE. Early observational work in the Milky Way suggested a common set of cloud properties described by the size–line-width relation, virial equilibrium, and constant surface density (Larson 1981; Solomon et al. 1987). Though supported by early extragalactic observations (Rosolowsky et al. 2003; Bolatto et al. 2008), subsequent observations revealed substantial variations in the properties of molecular clouds in the Galactic center (Oka et al. 2001; Shetty et al. 2012; Kruisjens & Longmore 2013; Walker et al. 2016; Kauffmann et al. 2017), the inner and outer Milky Way (Heyer et al. 2009; Rice et al. 2016; Miville-Deschênes et al. 2017), and across nearby star-forming galaxies (Donovan Meyer et al. 2013; Hughes et al. 2013a; Leroy et al. 2013a, 2015, 2016; Colombo et al. 2014; Sun et al. 2018). Meanwhile, starburst galaxies and merging systems have long been observed to show high surface and volume densities (e.g., Downes & Solomon 1998; Wilson et al. 2003, among many others). Today it is clear that there is no common set of cloud properties but that these systematically vary with galactic properties. We are still in the early stages of understanding how these variations in cloud properties affect a cloud’s SFE.

The turbulence-regulated models of star formation have been designed to match the SFRs found in (idealized) numerical simulations of ISM turbulence (Padoan & Nordlund 2011; Padoan et al. 2012; Federrath 2013, and many others). Their validation by observations remains inconclusive, however. The models agree with observations of (mostly low-mass) star-forming regions in the solar neighborhood (see compilations by Federrath & Klessen 2012; Hennebelle & Chabrier 2013; Krumholz 2014; Padoan et al. 2014). Subsequent studies of larger giant molecular cloud (GMC) samples in the Milky Way and the LMC revealed inconsistencies between the absolute SFR predicted by these models and observations. These studies also found significant scatter in the SFE of individual clouds, far in excess of what the models predict (these have been attributed to an accelerating SFR along a cloud’s time evolution), and only a weak dependence of the SFE on cloud properties (Murray 2011; Evans et al. 2014; Lee et al. 2016; Vutisalchavakul et al. 2016; Ochsendorf et al. 2017). Comparing cloud population averages to the SFR per \(H_2\) and \(\epsilon_{ff}\) in M51, Leroy et al. (2017a) also found a poor match to the predictions of turbulent models. The sense of the correlations between cloud properties and \(\epsilon_{ff}\) in M51 appears opposite that present in some of the models. They also found lower absolute values of \(\epsilon_{ff}\) than either the models or Galactic observations. A recent study of star formation in Galactic center clouds finds the turbulence-regulated models to agree with observations, but they also stress that the attempt to falsify the models is obstructed by the lack of consensus on the values of their free parameters (Barnes et al. 2017).

The above results demonstrate that we are still in the early stages of confronting turbulent models with observations, and the link between the disk equilibrium models and the cloud properties relevant to the turbulent models remains even less well understood. Extensive observational and theoretical work is required to establish the link between the galactic SFR, disk structure, cloud-scale gas properties, and star formation on the scale of individual clouds. In the coming years, we expect that uniform surveys of diverse environments with ALMA will play a major role in such experiments. For example, the ongoing PHANGS-ALMA survey\(^6\) (“Physics at High Angular-resolution in Nearby Galaxies with ALMA”; A. K. Leroy et al. 2019, in preparation) is mapping molecular gas via CO(2–1) emission at cloud scales in a large sample of 74 nearby star-forming galaxies. This allows for a uniform statistical analysis of ISM and cloud properties and their connection to star formation (Sun et al. 2018; Utomo et al. 2018; M. Chevance et al. 2019, in preparation).

At the moment, however, a valuable, largely untapped resource exists in the form of recent large surveys of molecular clouds in the Milky Way and the nearest galaxies. In this paper, we synthesize the current best-in-class single galaxy GMC studies, estimate the environments hosting the cloud populations, and compare them to theoretical expectations for the dynamical state and SFE of the gas. We present a literature compilation of galactic disk and molecular cloud properties for the Milky Way and seven local galaxies. We use these to address two main questions:

- **How does the dynamical state of the gas depend on environment?** We compare the cloud’s dynamical state (i.e., the observed virial parameter) to its expected value if the cloud is in pressure equilibrium with its local galactic environment. Similar comparisons have been performed, e.g., for dense clumps inside Galactic molecular clouds (Bertoldi & McKee 1992), for whole molecular clouds in the Milky Way (Field et al. 2011), and for the LMC, M33, and M51 (Hughes et al. 2013a, 2016). Here we extend this work to a sample of eight local galaxies broken into several discrete environments.

- **How does the apparent SFE per free-fall time \(\epsilon_{ff}\) relate to the properties of the local cloud population?** We relate mass-weighted average cloud properties to the gas depletion time \((M_{mol}/SFR)\) for each of our targets. We contrast these to the predictions of a suite of turbulence-regulated models of star formation as summarized in Federrath & Klessen (2012).

This synthesis should represent the most complete, most direct link between environment and cloud dynamical state, and the most general test of turbulent models of star formation to date.

We start by reviewing the virial theorem that defines the cloud’s dynamical state (Section 1.1) and the turbulent star formation

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\(^5\) In turbulent models, the SFE is typically defined as the fraction of molecular gas mass converted to stars over some fiducial timescale, which is usually the gravitational free-fall time.

\(^6\) For information on PHANGS, see http://phangs.org.
models (Section 1.2). Then, we present our literature compilation of galactic and cloud properties (Section 2, Table 1), link the cloud’s dynamical state to galactic environment (Section 3.1), and compare the SFR predicted by the turbulence-regulated models to the observed SFR (Sections 3.2 and 3.3). We conclude by giving an outlook on future work (Section 4) and summarizing our findings (Section 5).

1.1. Virial Theorem for Molecular Clouds

The energy balance and thus the dynamical state of a molecular cloud, is described by the virial theorem. For a nonmagnetized, isothermal, self-gravitating spherical cloud immersed in a uniform external medium, the virial theorem (e.g., Spitzer 1978)

$$\frac{1}{2} \frac{dI^2}{dt^2} = 2(T - T_\text{S}) + \mathcal{W}. \quad (1)$$

Here, $I$ is the moment of inertia within the cloud’s volume. The kinetic energy of the cloud is $2T = 3M\sigma^2$, with $\sigma$ being the one-dimensional velocity dispersion of the gas. The surface term of the kinetic energy is $2T_\text{S} = 4\pi R^3 P_\text{ext}$, where $P_\text{ext}$ refers to the ambient gas pressure. The self-gravitational binding energy of the cloud is $\mathcal{W} = -\frac{1}{2}GM^2\Sigma/\Gamma$, where $\Gamma$ is a geometrical form factor. $\Gamma = 0.6$ for a constant-density sphere (assumed here) and 0.73 for an isothermal sphere of maximal critical mass (Elmegreen 1989). The gravitational constant in our units is $G = 1/232.5 M_\odot^{-1}$ pc km s$^{-2}$.

The sign of $dI^2/dt^2$ determines whether the cloud will contract or expand, so that the balance of the terms on the right-hand side defines its imminent dynamical evolution. Following Bertoldi & McKee (1992, and many others), we use the dimensionless virial parameter

$$\alpha_{\text{vir, obs}} = \frac{2T}{|\mathcal{W}|} = \frac{\sigma^2}{\pi G M \Sigma} = \frac{P_{\text{int}}}{P_{\text{self}}} \quad (2)$$

to describe the relative importance of the cloud’s kinetic energy and gravitational energy. In a complementary way, we express the theoretically expected virial parameter for a cloud in pressure equilibrium with its ambient medium by

$$\alpha_{\text{vir, theo}} = 1 + \frac{2T_\text{S}}{|\mathcal{W}|} = 1 + \frac{P_{\text{ext}}}{P_{\text{self}}} \quad (3)$$

Here we have also defined the cloud’s internal kinetic pressure,

$$P_{\text{int}} = 3\rho\sigma^2, \quad (4)$$

and the pressure related to the cloud’s self-gravitational binding energy,

$$P_{\text{self}} = \frac{\Gamma}{2} \frac{\pi G \Sigma^2}{2}. \quad (5)$$

Here, $\Sigma$ refers to the mass surface density of the cloud.

We estimate the ambient midplane gas pressure from the weight of the gas in the combined gaseous and stellar potential, assuming vertical hydrostatic equilibrium (Elmegreen 1989, see also Blitz & Rosolowsky 2004; Ostriker et al. 2010; Field et al. 2011; Kim et al. 2013)

$$P_{\text{ext}} = \frac{\pi G \Sigma^2}{2} \left(1 + \frac{\sigma_{\text{ism}}}{\sigma_s} \frac{\Sigma_s}{\Sigma_{\text{ism}}}ight). \quad (6)$$

Here, $\Sigma_{\text{ism}}$ and $\Sigma_s$ are the average surface densities of the diffuse interstellar medium and stars, and the ratio $\sigma_{\text{ism}}/\sigma_s$ reduces the gravitational force exerted by stars onto the gas according to the differences in gaseous and stellar scale heights.

Following Ostriker et al. (2010) and Kim et al. (2013), we assume that the diffuse ISM provides the pressure onto molecular clouds. We calculate the average surface density of the diffuse ISM as

$$\Sigma_{\text{ism}} = \Sigma_{\text{atom}} + (1 - f_{\text{gmc}}) \Sigma_{\text{mol}}, \quad (7)$$

where $f_{\text{gmc}}$ is the fraction of molecular gas in the adopted GMC catalog (Table 1). This treatment assumes that all atomic gas is diffuse and that all GMCs are self-gravitating and so not part of the diffuse medium. Our treatment ignores the likely minor contribution of bound GMCs to the galactic disk potential (see Ostriker et al. 2010 for a complete treatment). We also assume that the contributions of cosmic rays and magnetic fields play a minor role in supporting the gaseous disk (see Elmegreen 1989).

1.2. Theories of Star Formation in Molecular Clouds

The turbulence-regulated star formation models predict the SFR in a galaxy or part of a galaxy by scaling the ratio of the cloud mass, $M_{\text{gmc}}$, and free-fall time, $\tau_\text{ff}$ by the SFE per free-fall time, $\epsilon_{\text{ff}}$.

$$\text{SFR} = \epsilon_{\text{ff}} \frac{M_{\text{gmc}}}{\tau_\text{ff}(\rho)}. \quad (8)$$

Here, the free-fall time is given by

$$\tau_\text{ff}(\rho) = \left(\frac{3\pi}{32G\rho}\right)^{1/2} \quad (9)$$

and is evaluated either at the mean cloud density or in a multiscale fashion at the volume density of each gas parcel inside the cloud.

We consider the models by Krumholz & McKee (2005, hereafter KM05), Padoan & Nordlund (2011, PN11), and Hennebelle & Chabrier (2012, HC11) in the form presented by Federrath & Klessen (2012, their Table 1; see also Padoan et al. 2014), as well as the simplified empirical fit to the PN11 model by Padoan et al. (2012, P12).

These models derive $\epsilon_{\text{ff}}$ by integrating the cloud’s density distribution to obtain the mass fraction above some critical density for collapse. That mass fraction is then compared to the free-fall time to generate a rate of star formation. The models differ on how the density distribution and the critical density for collapse depend on the mean physical properties of a cloud, i.e., the virial parameter ($\alpha_{\text{vir}}$), the sonic Mach number ($M$), the turbulence-driving parameter ($b$), and the relative strength of the thermal and magnetic pressure ($\beta$). They also differ regarding whether the free-fall time is calculated at a fixed density (single free-fall time models) or at the local density along the density distribution (multi-free-fall time models).

7 We note that the Krumholz & McKee model differs in KM05 and Federrath & Klessen (2012, FK12) in the definition of the sonic length scale $\lambda_s$; the former use the one-dimensional velocity dispersion while the latter use the three-dimensional one. Here we adopt the KM05 definition, implying SFEs per free-fall time that are a factor of $\sim$10 larger than those for the FK12 definition.

8 In this paper, we adopt three-dimensional Mach numbers.
# Galaxy and Cloud Properties

| Parameter | Unit | MW_CMZ | MW_5kpc | MW_10kpc | LMC | M33 | M31_6kpc | M31_11kpc | NGC 300 | M51_1kpc | M51_3kpc | NGC 253 | NGC 4526 |
|-----------|------|--------|---------|----------|-----|-----|----------|----------|---------|----------|----------|---------|---------|
| Dist      | Mpc  | 0.008  | 0.005   | 0.005    | 0.05 | 0.84 | 0.78     | 0.78      | 1.90    | 7.60     | 7.60     | 3.50    | 16.40   |
| log $M_*$ | $M_\odot$ | 9.15  | 10.76   | 10.76    | 9.30 | 9.70 | 11.00    | 11.00     | 9.30    | 10.56    | 10.56    | 10.33   | 10.97   |
| log $M_{star}$ | $M_\odot$ | ...  | 9.90    | 9.90     | 8.80 | 9.10 | 9.90     | 9.90      | 9.30    | 9.45     | 9.45     | 9.45    | 9.45    |
| log $M_{mol}$ | $M_\odot$ | 7.30  | 9.17    | 9.17     | 7.80 | 8.50 | 8.80     | 8.80      | 8.10    | 9.82     | 9.82     | 8.55    | 8.59    |
| log SFR | $M_\odot$ yr$^{-1}$ | −1.05 | 0.22    | 0.22     | −0.70 | −0.35 | −0.60    | −0.60     | −0.72   | 0.47     | 0.47     | 0.62    | −0.76   |

| Parameter | Unit | Galaxy Properties |
|-----------|------|-------------------|
| $R_{gal}$ | kpc  | 0−0.12 (99)       |
| $v_{C,star}$ | km s$^{-1}$ | 100.0 (87)       |
| $v_{C,gas}$ | km s$^{-1}$ | 15.0 (74)       |
| $\Sigma_{g}$ | $M_\odot$ pc$^{-2}$ | 3800.0 (74) |
| $\Sigma_{atom}$ | $M_\odot$ pc$^{-2}$ | ... |
| $\Sigma_{mol}$ | $M_\odot$ pc$^{-2}$ | 10000.0 (49) |
| $\Sigma_{d}$ | $M_\odot$ pc$^{-2}$ | 4500.0 (4) |
| $\tau_{dep}$ | Gyr$^{-1}$ | 0.22 (4) |

| Parameter | Unit | Local Cloud Properties |
|-----------|------|------------------------|
| $F_{gmc}$ | pc   | 0.10 (49)              |
| $R$      | pc   | 2.2 (49)               |
| $v_{in}$ | km s$^{-1}$ | 5.87 (49) |
| $M_{10^9}$ | $M_\odot$ | 0.01 (49) |
| $M_{10^6}$ | $M_\odot$ | 0.09 (49) |
| $\tau_{cross}$ | Myr | 0.22 (49) |
| $\tau_{fit}$ | Myr | 0.44 (49) |

| Parameter | Unit | Local Cloud Properties |
|-----------|------|------------------------|
| log $P_{out}$ | K cm$^{-3}$ | 7.74 |
| log $P_{out}$ | K cm$^{-3}$ | 6.65 |
| log $P_{out,star}$ | K cm$^{-3}$ | 7.23 |
| log $P_{out,gas}$ | K cm$^{-3}$ | 7.43 |

**References.** (2) Amblard et al. (2014), (4) Barnes et al. (2017), (8) Bland-Hawthorn & Gerhard (2016), (13) Bovy & Rix (2013), (14) Braun et al. (2009), (16) Caldi-Primo et al. (2013), (19) Ciardullo et al. (2002), (22) Dalcanton et al. (2012), (24) Davis et al. (2014), (26) Dorman et al. (2015), (28) Draud et al. (2014), (39) Ford et al. (2013), (43) Gieren et al. (2004), (44) Gratier et al. (2010), (49) Henshaw et al. (2016), (50) Heyer & Dame (2015), (56) Hughes et al. (2013a), (60) Iodice et al. (2014), (61) Jameson et al. (2016), (62) Kalberla & Kerp (2009), (63) Kam et al. (2015), (64) Kang et al. (2016), (66) Kennicutt & Evans (2012), (74) Kruisje et al. (2014), (87) Lauerhardt et al. (2002), (90) Leroi et al. (2008), (93) Leroy et al. (2015), (97) Licquia & Newman (2015), (98) Licquia & Newman (2016), (99) Longmore et al. (2013), (101) Lucero & Young (2013), (104) Lucero et al. (2015), (102) Meidt et al. (2013), (106) Mothis-Mateos et al. (2007), (107) Muñoz-Mateos et al. (2015), (110) Nakanishi & Sofue (2016), (111) Nieto et al. (2006), (120) Petty et al. (2013), (122) Rekola et al. (2005), (124) Rice et al. (2016), (132) Sanders et al. (2003), (136) Schuba et al. (2010), (137) Schuba et al. (2012), (135) Schuba et al. (2019, this work), (134) A. Schuba et al. (2019, in preparation), (139) Schuster et al. (2007), (140) Seigar (2011), (144) Skibba et al. (2012), (145) Sofue & Nakanishi (2016), (148) Staveley-Smith et al. (2003), (152) Tam et al. (2012), (153) Tomiy in et al. (2001), (156) Utomo et al. (2015), (159) Verley et al. (2009), (164) Westmeier et al. (2011), (168) Wong et al. (2009), (171) Young et al. (2011), (158) van der Marel et al. (2002). (This table is available in its entirety in machine-readable form.)
To compare the models with observations, we need to choose values of their free parameters. Here, we adopt the fiducial parameters from the original works: \( \epsilon_{\text{core}} = 0.5 \), \( \phi_{\ell} = 1.91 \), \( \phi_{\chi} = 1.12 \), \( \theta = 0.35 \), and \( \chi_{\text{cut}} = 0.1 \). Note that Federrath & Klessen (2012) derived significantly different values for these parameters using magnetohydrodynamical turbulent box simulations. We adopt the following default cloud properties: \( \mathcal{M} = 10 \), typical for modestly supersonic molecular gas (Padoan et al. 2014) and Milky Way GMCs (Heyer et al. 2009); \( b = 0.4 \), found for a mix of solenoidal and compressive forcing (Federrath et al. 2010); and negligible magnetic fields, \( \beta \rightarrow \infty \) (Crutcher 2012). We will also consider the effect of varying these quantities about their default values. We treat the virial ratio as known, determined by observations.

2. Data

Table 1 presents our compilation of galaxy- and cloud-scale measurements. Together these allow us to assess (a) the relationship between the cloud’s dynamical state and local galactic environment and (b) SFE per free-fall time as a function of the local cloud population.

As the table shows, surveys of the molecular gas with resolution to study individual molecular clouds now cover a suite of individual nearby galaxies. Compared to the first studies targeting the Local Group (see review by Fukui & Kawamura 2010), these have improved resolution and sensitivity, and span a larger range of environments within galaxies. We combine surveys of the LMC (using MOPIRA; Wong et al. 2009), M33 (using the IRAM 30-m; Gratier et al. 2010; Dray et al. 2014), M31 (using CARMA; Caldú-Primo & Schruba 2016; A. Schruba et al. 2019, in preparation), the lenticular galaxy NGC 4526 (Utomo et al. 2015), M51 (using NOEMA; Pety et al. 2013; Schinnerer et al. 2013), the central starburst in NGC 253 (Leroy et al. 2015), and the nearby dwarf spiral NGC 300 (Kruisjes et al. 2019b; A. Schruba et al. 2019, in preparation).

2.1. Galaxy Properties

Our galaxy sample comprises eight local galaxies spanning a wide range of stellar masses and morphologies. We include one dwarf irregular: the LMC, two low-mass spirals: M33 and NGC 300, two massive spirals: the Milky Way and M51, one starburst galaxy center: NGC 253, one green-valley galaxy: M31, and one lenticular galaxy: NGC 4526.

We compile global measurements of the stellar mass (\( M_* \)), atomic (\( M_{\text{gas}} \)) and molecular gas mass (\( M_{\text{mol}} \)), and SFR from the literature, or we derive them from our own data. Our sample covers about two orders of magnitude in various host galaxy properties: \( M_* = 2 \times 10^8-10^{11} \ M_{\odot} \), SFR = 0.03–4.2 \( M_{\odot} \) yr\(^{-1} \), sSFR = 2 \( \times 10^{-12}–2 \times 10^{-10} \) yr\(^{-1} \), and \( f_{\text{gas}} = M_{\text{gas}}/(M_{\text{gas}}+M_*) = 0.01–0.5 \).

We subdivide our galaxies into local galactic environments, separating central regions, inner disks, and outer disks. These different regions have different surface densities and ISM properties, which may affect the cloud properties and SFE. Table 1 presents the local environments for each target.

For each environment, we determine the local galactic properties at the median galactocentric radius of the respective cloud sample (see below). We use radial profiles of each tracer, with their total flux pinned to the global properties, to determine the surface densities of stars (\( \Sigma_* \)), atomic (\( \Sigma_{\text{atom}} \)) and molecular gas (\( \Sigma_{\text{mol}} \)), SFR (\( \Sigma_{\text{sfr}} \)), and the (vertical) velocity dispersions of the stellar and gaseous disks (\( \sigma_* \) and \( \sigma_{\text{gas}} \)).

The range of local galactic properties is even broader than the range of global ones. Our sample covers \( \Sigma_* = 25–4000 \ M_{\odot} \) pc\(^{-2} \), \( \Sigma_{\text{atom}} = 3–18 \ M_{\odot} \) pc\(^{-2} \), \( \Sigma_{\text{mol}} = 2–1000 \ M_{\odot} \) pc\(^{-2} \), \( \Sigma_{\text{dust}} = 1.5–3500 \ M_{\odot} \) pc\(^{-2} \) Gyr\(^{-1} \), and molecular depletion time \( \tau_{\text{dep}} = 0.2–4.4 \) Gyr. From these local galactic properties, we derive the ambient gas (midplane) pressure, \( P_{\text{amb}} \), as defined in Section 1.1.

2.2. Cloud Properties

These extragalactic surveys approach the detail of the CfA-Chile survey of the Milky Way (Dame et al. 2001; \~{}30 pc at the Galactic Ring), typically with sensitivity to clouds with molecular gas mass as low as \( \sim 10^3–10^5 \ M_{\odot} \). They use different telescopes and achieve different physical resolution and sensitivity, and in some cases use different tracers of the molecular gas. As a result, our combined data set is heterogeneous in nature.

Whenever we had access to the original data sets, we extracted the measurements ourselves. We use an updated version of the CPROPS code\(^9\) (Rosolowsky & Leroy 2006; Leroy et al. 2015). The code identifies emission peaks with signal-to-noise ratio \( \geq 5 \) in two adjacent channels. Then it assigns adjacent pixels to an emission peak until an intensity level is reached where the pixel cannot be uniquely assigned to one peak. Finally, the properties of a cloud are determined from the intensity-weighted moments. These are corrected for the effects of blending and finite sensitivity assuming that the cloud can be approximated as a three-dimensional Gaussian. Then the measured size and line width are corrected for the intrinsic spatial and spectral resolution of the data.

When the original data were not available or re-extraction was not feasible, we adopt the literature measurements scaled to our assumed distances.

We define the macroscopic cloud properties as follows:

\[
\text{Radius: } R = 1.91 \sqrt{\sigma_* \sigma_v} \quad (10)
\]

\[
\text{Luminous Mass: } M = \alpha_{\text{CO}} L_{\text{CO}} \quad (11)
\]

\[
\text{Virial Mass: } M_{\text{vir}} = \frac{5\sigma^2 R}{G} \quad (12)
\]

\[
\text{Surface Density: } \Sigma = 0.77 \frac{M}{\pi R^2} \quad (13)
\]

\[
\text{Volume Density: } \rho = 1.26 \frac{M}{4/3 \pi R^3} \quad (14)
\]

We note that all masses and densities in this paper include the contribution of heavy elements. \( \sigma_* \) and \( \sigma_{\text{gas}} \) in Equation (10) denote the size of a cloud (defined by the intensity-weighted second moment along the two spatial axes).

From these macroscopic cloud properties we derive the cloud’s free-fall time, \( \tau_{\text{ff}} \), and turbulent crossing time, \( \tau_{\text{cross}} = R/\sqrt{3} \sigma_{\text{g}} \) (for one-dimensional velocity dispersions), as well as the cloud’s internal turbulent pressure, \( P_{\text{int}} \), and the self-gravitational pressure, \( P_{\text{self}} \), as defined in Equations (4)–(5).

We note that the definitions of the macroscopic cloud properties (Equations (10)–(14)) and the definitions of the cloud virial parameter and internal pressures (Equations (2)–(5)) bear minor inconsistencies in the geometric factors describing the density distribution of the molecular clouds, i.e., constant, \( 1/r \), or Gaussian density profiles. For now we accept this to match common definitions and account for these differences as part of

\(^9\) https://github.com/akleroy/cpropstoo
the systematic uncertainties (see below). In the future, we intend to remedy this inconsistency by determining the geometric factors from higher dynamic range data obtained with ALMA.

To derive molecular cloud masses, we adopted the standard Galactic CO(1–0) to H$_2$ conversion factor: $\alpha_{\text{CO}} = 4.35 \, M_{\odot} \, \text{pc}^{-2} \, (\text{K km s}^{-1})^{-1}$ (which includes a correction for heavy elements) for the Milky Way disk, M31, M51, and NGC 4526; for the low-mass galaxies LMC, M33, and NGC 300, we adopt twice this value (Wong et al. 2011; Druard et al. 2014; Kruĳssen et al. 2019b). For M33, we further adopt a CO(2–1) to CO(1–0) brightness temperature ratio of 0.8 (Druard et al. 2014). For the Milky Way center and NGC 253, molecular gas masses are derived from optically thin dense gas tracers and dust continuum (Leroy et al. 2015; Walker et al. 2015).

The above method to calculate cloud properties remedies as best as possible the signatures of inhomogeneous resolution and sensitivity between our different data sets. Despite this effort, we note that peak identification methods such as CPROPS naturally tend to identify structures with size similar to the native resolution of the data set (Table 1; see also Leroy et al. 2016).

For each of the local galactic environments defined in Section 2.1 and Table 1, we derive mass-weighted average cloud properties. We note that for the calculation of the mass-weighted averages, the order in which cloud properties and averages are calculated matters. We calculate all macroscopic cloud properties (Equations (10)–(14), the pressure-related quantities and thereof derived “observed” and “predicted” virial parameters (Equations (2)–(6)) for each cloud individually and then determine their mass-weighted average. We test whether our results depend on this methodology by calculating the virial parameter and pressure quantities from mass-weighted average cloud properties instead and find no major difference.

This sample-averaging resembles the methodology described in Leroy et al. (2016) and distinguishes our work from previous studies. Appropriate averaging over all clouds in a galactic environment highlights the impact of environment on the mean cloud properties. Previous studies have plotted the entire cloud population, often emphasizing offsets among scaling relations. This shows the full dynamic range of cloud properties (which is frequently interpreted to reflect the time evolution of the clouds; e.g., Murray 2011; Lee et al. 2016; Padoan et al. 2017) but can obscure the dependence of cloud properties and star formation on environment.

Our study also expands the range of galactic environments for which cloud properties and star formation models have been tested. Most work so far has focused on single targets, either the Milky Way (Field et al. 2011; Murray 2011; Vutisalchavakul et al. 2016; Barnes et al. 2017) or individual selected local galaxies (Utomo et al. 2015; Leroy et al. 2017a; Ochsendorf et al. 2017; Schruba et al. 2017). The best synthetic work today, by Hughes et al. (2013a), had only three high-quality data sets available.

2.3. Uncertainties and Error Propagation

We account for uncertainties in the cloud properties, their sample averages, and the galactic disk parameters. We consider (a) statistical uncertainties due to finite signal-to-noise ratios (S/N) and uncertain sensitivity corrections, (b) statistical uncertainties due to sample variance when determining the mass-weighted averages, and (c) systematic uncertainties in the mass-to-light conversion factors and the adopted geometric factors.

Because the statistical uncertainties in the cloud properties are not always available (from the literature), we adopt typical uncertainties derived from in-hand data sets. We estimate these based on our application of the CPROPS code to cases where we have the original data cube (including extrapolations to the zero noise level; see Rosolowsky & Leroy 2006; Leroy et al. 2015; and the CPROPS documentation). For our typical case of marginally resolved clouds detected at peak S/N ~ 5–10, we find logarithmic uncertainties of 0.1 dex for $R$; 0.15 dex for $\alpha_I$; 0.25 dex for $M_{\text{vir}}$; 0.3 dex for $M_{\text{sum}}$, $\Sigma$, and $\tau_{\text{vir}}$; and 0.35 dex for $\alpha_{\text{vir}}$.

We derive uncertainties in the (mass-weighted) averages using a Monte Carlo analysis, which accounts for (i) sample variance by bootstrapping and (ii) statistical uncertainties by perturbing the cloud properties. In this work, we do not study resolution or completeness effects but work with the best current data at their native resolution. We plan to investigate these effects in the future. See Sun et al. (2018) for more analysis of the possible impact of these factors.

Many of our calculations rely on knowledge of the mass of gas or stars. These are affected by systematic uncertainty in the light-to-mass conversion. For the CO-to-H$_2$ conversion factor, we adopt an uncertainty of 0.2 dex for massive galaxies. For smaller galaxies, with metallicity $Z \lesssim 0.5 Z_\odot$ (i.e., LMC, M33, NGC 300), we treat the CO-to-H$_2$ conversion factor as uncertain by 0.3 dex. For the 3.6 $\mu$m-to -$M_*$ factor, we adopt a fixed uncertainty of 0.15 dex.

Different assumptions in cloud geometries (e.g., constant, $1/r$, or Gaussian density profiles) lead to additional systematic uncertainties of 0.15 dex in radius and 0.10 dex in line width. We analytically (or numerically for the sample averages) propagate the uncertainties from the input parameters to the derived parameters.

Note that we do not account for the covariance among the uncertainties. This implies that our quoted uncertainties represent conservative upper limits.

In general, we find that the statistical uncertainties on the properties of individual molecular clouds are significantly suppressed by our approach of determining sample averages and often reduce to $\lesssim 0.05$–0.10 dex, with the exception of galactic environments with very small cloud catalogs (i.e., NGC 253). Therefore, the systematic uncertainties dominate our formal error budget. However, we note that these systematic uncertainties are expected to bias parameters in the same way for many/all galaxies in our sample, and thus should again be interpreted as conservative upper limits on the uncertainties. In the following figures, we show these two types of uncertainties: colored error bars account for all sources of uncertainties except for systematic ones, whereas gray error bars also include systematic uncertainties.

3. Results

In Table 1, we present our compilation of cloud properties in context for the Milky Way and seven local galaxies. The table includes global galaxy properties that describe our galaxy sample and can be used to reference to other samples. The local galaxy properties give the galactic disk properties at the median galactocentric radius of our cloud sample; these quantities set the ambient medium pressure and the molecular gas depletion time. The local cloud properties list the mass-weighted mean
properties of the cloud population and the fraction of molecular mass in each cloud catalog. The pressure parameters state the mass-weighted clouds’ turbulent and self-gravitational pressures, and the ambient medium pressures by the stellar and gaseous disks. We use these measurements to study the dependence of the clouds’ dynamical state on local galactic environment, to assess their SFE, and to test theories of star formation in turbulent clouds.

3.1. Dynamical State of Molecular Clouds and Its Dependence on Galactic Environment

Figure 1 illustrates the relationship between the dynamical state of molecular clouds and local galactic environment. The \( x \)-axis shows the virial parameter, \( \alpha_{\text{vir}} \), (Equation (2)) derived from the observed balance of the clouds’ kinetic and self-gravitational pressures (Equations (4)–(5)). The \( y \)-axis shows the values of \( \alpha_{\text{vir}} \) predicted for virialized clouds in external pressure equilibrium (Equation (3)). Data points show the mass-weighted average of the cloud population for each region that we study (Section 2.2). Error bars represent the statistical uncertainties and sample variance (in color) and also include systematic uncertainties (in gray). The color-coding shows whether atomic or molecular gas dominates the ISM. Virialized clouds confined only by self-gravity lie along the vertical dashed line, and those confined by external pressure along the diagonal dotted line.

Figure 1. Virial parameter, \( \alpha_{\text{vir}} \), of molecular clouds derived from the observed balance of the clouds’ kinetic and self-gravitational pressures (\( x \)-axis) and as predicted for virialized clouds in external pressure equilibrium (\( y \)-axis). Data points show the mass-weighted average of the cloud population of an entire galaxy or a distinct subregion therein. Error bars represent the statistical uncertainties and sample variance (in color) and also include systematic uncertainties (in gray). The color-coding shows whether atomic or molecular gas dominates the ISM. Virialized clouds confined only by self-gravity lie along the vertical dashed line, and those confined by external pressure along the diagonal dotted line.

To first order, “self-gravitating” clouds have high surface densities (\( \Sigma_{\text{gmc}} \approx 10^{2}–10^{4} \, M_{\odot} \, pc^{-2} \)) and are found in high ambient pressure environments (\( P_{\text{ext}} \approx 4 \times 10^{7}–7 \times 10^{8} \, K \, cm^{-3} \)) as in the central and inner Milky Way, M51, NGC 253, and NGC 4526. Despite the high ambient pressure in their environments, these clouds appear nearly virialized considering only their self-gravity and internal motions.\(^{10}\)

High virial parameter, (externally) pressurized clouds have low surface densities (\( \Sigma_{\text{gmc}} \approx 10–30 \, M_{\odot} \, pc^{-2} \)) and reside in low ambient pressure environments (\( P_{\text{ext}} \approx 5 \times 10^{3}–3 \times 10^{5} \, K \, cm^{-3} \)) as in the outer Milky Way, LMC, M31, M33, and NGC 300. These clouds appear virialized only once external pressure terms are taken into account.

The dependence of the clouds’ virial parameters on their surface densities is also apparent when considering clouds of different kinetic pressure, \( P_{\text{int}} \), and external pressure \( P_{\text{ext}} \). In our data, both of these pressure scalings exhibit a dispersion of \( \sim 0.5 \, \text{dex} \). That scatter in the pressure–pressure scalings appears to originate from a systematic trend between \( P_{\text{int}}/P_{\text{ext}} \) with \( P_{\text{int}} \).

Put another way, Figure 1 implies that molecular clouds in local galaxies are in virial equilibrium once the confining external pressure is accounted for (i.e., diagonal dotted line). But they are not necessarily in a simple virial equilibrium set only by the clouds’ self-gravity (i.e., vertical dashed line). The local galactic environment has a clear and substantial imprint on the dynamical state of molecular clouds. We find the (sample-averaged) virial parameter to have a large (factor \( \sim 15 \)) systematic variation among our galaxies and distinct subregions therein, and we find that these variations are significantly larger than all sources of uncertainty. In some environments, clouds have virial parameters near unity (i.e., the bottom-left part of Figure 1). These clouds appear virialized; considering only their self-gravity and external pressure has no major impact. In other environments, clouds have virial parameters of \( \sim 3–10 \) (i.e., the top-right part of Figure 1), indicating these clouds have kinetic energies much larger than their self-gravitational energies. These clouds are either unbound and transient, or they are pressure-confined.

These systematic variations in the dynamical state of molecular clouds link to properties of the local galactic environment. We qualitatively break our sample into two classes of clouds, living in two different types of environments. We list the approximate properties of these two classes in Table 2.

| Property | Pressurized | Self-gravitating |
|----------|------------|-----------------|
| \( P_{\text{ext}} \) [K \, cm\(^{-3}\)] | \( 5 \times 10^{3}–3 \times 10^{5} \) | \( 4 \times 10^{4}–7 \times 10^{7} \) |
| \( \Sigma_{\text{gmc}} \) \([M_{\odot} \, pc^{-2}]\) | 25–170 | 200–4000 |
| \( \Sigma_{\text{gmc}} \) \([M_{\odot} \, pc^{-2}]\) | 10–23 | 17–10^{3} |
| \( R_{\text{ext}} \) | 0.1–0.7 | 5–200 |
| \( \Sigma_{\text{gmc}} \) \([M_{\odot} \, pc^{-2}]\) | 10–30 | 10^{-3}–10^{4} |
| \( \alpha_{\text{vir, obs}} \) | 3–10 | 0.7–3 |

Note. The table lists the full range of the environmental (top) and cloud (bottom) properties for the two classes of clouds and galactic environments (see text).

\(^{10}\) For the Galactic center, we only consider clouds on the “dust ridge” of the “100 pc stream” (Walker et al. 2015), which contains the highest-density clouds in the region. For clouds at larger galactocentric radii, we expect a larger influence of the external pressure (e.g., Kruijssen et al. 2014).
masses. To investigate this, we considered subsamples of clouds with masses within logarithmic bins between $10^4 M_\odot$ and $10^7 M_\odot$. We find that lower mass clouds ($M_{\text{gmc}} = 10^4$–$10^5 M_\odot$) have high virial parameters ($\alpha_{\text{vir}} \approx 2$–$10$), while massive clouds ($M_{\text{gmc}} = 10^5$–$10^7 M_\odot$) have low virial parameters ($\alpha_{\text{vir}} \approx 1$–$3$). One can thus say that the more massive a cloud is, the more likely it is to have high surface density and therefore decouple dynamically from its environment. However, the threshold when this decoupling sets in is a strong function of the density of clouds’ ambient medium (see also Meidt et al. 2018; S. E. Meidt et al. 2019, in preparation).

The color-coding in Figure 1 highlights one major difference distinguishing the environments where the two classes of clouds are found. Color indicates whether the ISM is predominantly composed of atomic or molecular gas. The figure shows that the “pressurized” clouds are more likely to be found in parts of galaxies where atomic gas makes up most of the neutral interstellar medium.

Such systematic variations in cloud properties with environment have been suggested by molecular cloud surveys in the inner and outer Milky Way (Heyer et al. 2001, 2009; Field et al. 2011) and seen contrasting M33, M51, and the LMC by Hughes et al. (2013b, 2016). Here, we roughly triple the sample of galaxies studied and synthesize Milky Way measurements and extragalactic work. This larger data set clearly shows that the dynamical state of molecular clouds depends on environment in a systematic way.

Our results also agree with recent works by Leroy et al. (2016) and Sun et al. (2018). Those papers present a similarly large dynamic range in the virial parameters of molecular gas in nearby galaxies. They adopted the pixel-based analysis method developed by Leroy et al. (2016) and measured the gas surface density and line width at fixed spatial scales of $\sim45$–$120$ pc, which with an assumption on the beam filling factor and the gas extent along the line of sight traces the virial parameter. They also found that molecular gas in massive, molecular-gas-dominated spiral galaxies has $\alpha_{\text{vir}} \sim 2$ (i.e., energy equipartition) while the gas-poor, atomic-gas-dominated galaxies M31 and M33 have $\alpha_{\text{vir}} \sim 3$–$10$. This agreement is partially by construction, because Leroy et al. (2016) and Sun et al. (2018) analyzed the same M31, M33, and M51 data that we consider here.

Sun et al. (2018) suggest several possible drivers for the high apparent $\alpha_{\text{vir}}$ in M31 and M33 including (a) beam dilution of molecular clouds much smaller than their 45–80 pc measurement scale or (b) the impact of the ambient pressure from the interstellar medium (as we argue here). In this work, we require emission peaks to be (at least marginally) spatially resolved to directly measure their size, line width, and surface densities. Our CPROPS methodology has its own biases, as it tends to find beam-sized objects and leads to incompleteness in the measurements. But our measurements offer a strong indication that even resolved clouds in these galaxies appear “pressurized,” so that beam dilution is not the sole reason for the high $\alpha_{\text{vir}}$ values. We argue that these high virial parameters are indeed a sign of pressure confinement by the diffuse ambient medium in atomic-gas dominated galaxies like M31, M33, NGC 300, and the LMC.

Moreover, Figure 1 provides substantial evidence in favor of the hypothesis by Elmegreen (1989) that the cloud’s dynamical state is linked to the ambient gas pressure set by the vertical hydrostatic equilibrium (Equation (6)). However, our definition of $P_{\text{ext}}$ differs from Elmegreen’s one by a constant and in only considering the diffuse ISM to provide the ambient gas pressure in the midplane (Equation (7)). A number of alternative expressions for the ambient pressure confining molecular clouds have been proposed (Chieze 1987; Bertoldi & McKee 1992; Wolfire et al. 2003; Blitz & Rosolowsky 2006; Koyama & Ostriker 2009; Ostriker et al. 2010; Kim et al. 2011, and others). These expressions differ in assumptions on the structure of the ISM, the size of atomic-shielding layers around molecular clouds, the effect of magnetic fields, and the scale height of cosmic rays, leading to predictions of the ambient gas pressure that differ by a factor of a few. Unfortunately, these differences are comparable to the systematic uncertainties in our measurements of the cloud and environmental parameters, which precludes a firm conclusion as to which expression matches our observations best (see also Hughes et al. 2016). We will investigate this topic in more detail using sensitive cloud-scale mapping of the molecular gas obtained by the PHANGS-ALMA survey.

3.2. SFE of Molecular Clouds and Whole Galaxies

We also infer the SFR and molecular gas depletion time for each region studied. By comparing this to the average cloud properties, we can compare these against measurements of the SFE on galactic scales and predictions of star formation theories in the literature (Section 3.3).

Figure 2 shows the SFE per dynamical time, $\epsilon_{\text{dyn}}$, as a function of the virial parameter, $\alpha_{\text{vir}}$. $\epsilon_{\text{dyn}} = \tau_{\text{dyn}}/\tau_{\text{dep}}$ is the ratio of the local dynamical timescale, $\tau_{\text{dyn}}$, to the global molecular gas depletion timescale, $\tau_{\text{dep}} = M_{\text{mol}}/\text{SFR}$, determined over the range of galactocentric radii of the cloud populations. Thus, $\epsilon_{\text{dyn}}$ expresses the fraction of molecular gas converted to stars per dynamical timescale. $\epsilon_{\text{dyn}}$ represents a slight generalization of the $\epsilon_{\text{f}}$ discussed in Section 1.2, which treated the gravitational free-fall time as $\tau_{\text{ff}}$.

In Figure 2, each data point shows the mass-weighted average of the cloud population for one of our regions. For each region, we show two data points that consider different local dynamical timescales, $\tau_{\text{dyn}}$, i.e., either the free-fall time, $\tau_{\text{ff}}$ (diamond symbols), or the turbulent crossing time, $\tau_{\text{cross}}$ (square symbols). For the points adopting $\tau_{\text{dyn}} = \tau_{\text{ff}}$, we also show the statistical uncertainty including sample variance (colored error bars) and the full uncertainty range also including systematic uncertainty (gray error bars). The uncertainties for the data points including $\tau_{\text{cross}}$ are comparable, but omitted for clarity. As in Figure 1, data points are color-coded to indicate whether atomic or molecular gas dominates the ISM. All data values shown here can be found in Table 1. The top axis of the figure re-expresses the virial parameter, $\alpha_{\text{vir}}$, as $\left(\tau_{\text{ff}}/\tau_{\text{cross}}\right)^2 = \pi^2 \alpha_{\text{vir}}^2/8$, adopting our fiducial $\Gamma = 0.6$.

Low SFE per dynamical time: Figure 2 shows that (i) $\epsilon_{\text{dyn}}$ varies between 0.05%–3%, (ii) these variations are much larger than any source of uncertainty (and are therefore real), and (iii) there is no strong difference whether $\tau_{\text{dyn}}$ is set to $\tau_{\text{ff}}$ or $\tau_{\text{cross}}$.

11 We do not reduce the total midplane gas pressure by the relative contributions from cosmic rays and magnetic fields, for which Elmegreen (1989) assumed relative contributions of 0.40 and 0.25, respectively. Instead, we assume the vertical scale height of cosmic rays and magnetic fields to be larger than the scale height of the neutral gas, such that they have a minimal stabilizing effect on the weight of the neutral gas disk.

12 The diffuse ISM mass is defined as the total neutral gas mass minus the gas mass within molecular clouds, i.e., we assume a minor contribution of molecular clouds to the galactic disk potential (e.g., Ostriker et al. 2010).

8
The values of $\epsilon_{\text{dyn}}$ are low in an absolute sense, with only 0.1%–1% of the molecular gas mass converted to stars per collapse time. They are in good agreement with previous studies connecting cloud-scale $\tau_{\text{vir}}$ to the disk-averaged $\tau_{\text{dep}}$ in the Milky Way (Murray 2011; Vutisalchavakul et al. 2016), in M51 (Leroy et al. 2017a), or in a sample of massive spiral galaxies (Utomo et al. 2018). Our measurements are also in good agreement with studies of the kiloparsec-scale distribution of dense gas, bulk molecular gas, and recent star formation in samples of nearby galaxies (García-Burillo et al. 2012; Usero et al. 2015). They are often but not always lower than the typical $\epsilon_{\text{ff}} \sim 0.5\%$–2% found by studies focused on Galactic star-forming clouds (Evans et al. 2014; Heyer et al. 2016; Lee et al. 2016; Barnes et al. 2017)—a discrepancy that we attribute to their selection bias on currently star-forming clouds while ignoring quiescent clouds that dominate the molecular gas budget on Galactic scales (see Section 3.2.3 in Leroy et al. 2017a). Our results are significantly ($\sim 25 \times$) smaller than the recent measurement of $\epsilon_{\text{ff}} \sim 5\%$–25% for star-forming clouds in the LMC (Ochsendorf et al. 2017). The underlying cause for this difference remains unclear; however, the short global molecular gas depletion time of the LMC ($\tau_{\text{dep}} \approx 0.4$ Gyr; Jameson et al. 2016) likely plays a role.

**Scatter and systematic trend in the SFE per dynamical time:**

In addition to the overall low $\epsilon_{\text{ff}}$, we also find a nearly two-order-of-magnitude large dynamic range in $\epsilon_{\text{ff}}$. Despite this large scatter in our full sample, our previous differentiation between clouds in low- and high-pressure environments (or equivalently between atomic- or molecular-gas-dominated regions as highlighted by the color-coding of data points) suggests that molecular clouds in low-pressure, atomic-dominated regions (the orange-red symbols) follow a common trend between $\epsilon_{\text{dyn}}$ and $\alpha_{\text{vir}}$ such that regions with small virial parameter ($\alpha_{\text{vir}} \sim 1$–3) have the largest observed SFE per free-fall time ($\epsilon_{\text{ff}} \sim 1\%$–3%), while clouds with large virial parameter ($\alpha_{\text{vir}} \sim 5$–10) have systematically lower SFE per free-fall time ($\epsilon_{\text{ff}} \sim 0.1\%$–0.7%). For the other class of clouds living in high-pressure, molecular-dominated regions (the blue symbols), we observed among the lowest values for the SFE per free-fall time ($\epsilon_{\text{ff}} \sim 0.05\%$–0.5%) and found no clear trend with the clouds’ virial parameters.

A large dynamic range in $\epsilon_{\text{ff}}$ has been measured by studying individual clouds in the Milky Way and the LMC (Lee et al. 2015; Murray & Chang 2015; Ochsendorf et al. 2017). These variations have been interpreted as the evolution of individual clouds. But our measurements average over large areas and many molecular clouds in distinct evolutionary states. They must reflect systematic differences among our targets.

**Free-fall or crossing time as fiducial timescale of gravitational collapse and star formation:**

The models of turbulence-regulated star formation discussed in Section 1.2 motivate the free-fall time to be the relevant timescale for star formation. While we do find $\tau_{\text{dep}}$ to be correlated with $\tau_{\text{ff}}$, we note that the correlation of $\tau_{\text{dep}}$ with $\tau_{\text{cross}}$ is equally strong. This finding paired with the large scatter in $\epsilon_{\text{ff}}$ does not support the view that the gravitational free-fall time alone is a reliable predictor of the SFR of real molecular clouds in the disk of galaxies—in addition $\tau_{\text{cross}}, \alpha_{\text{vir}}$, and other physical parameters are seen to play an important role. The common assumption (especially in numerical simulations) of a constant SFR per free-fall time of order $\epsilon_{\text{ff}} \sim 1\%$–10% with small 0.4 dex scatter (e.g., Krumholz & Tan 2007) does not seem to hold universally across all galactic environments present in the nearby galaxy population.

As discussed above, this conclusion agrees with work studying individual systems, which have raised similar concerns about the predictive power of $\tau_{\text{ff}}$.

**Role of diffuse molecular gas:** Our calculation of $\epsilon_{\text{dyn}}$ depends on the ability to compare the integrated molecular gas depletion time to timescales derived from the resolved cloud population. This could potentially be complicated by any non-stellar-forming, diffuse molecular gas. Evidence for diffuse molecular gas comes from studies of the spatial and spectral distribution of CO emission in galaxies which estimate it to account for $\lesssim 50\%$ of the total molecular gas (e.g., Caldú-Primo et al. 2013; Pety et al. 2013; Caldú-Primo & Schruba 2016; Roman-Duval et al. 2016; see also Hygate et al. 2019, who propose a new, physically motivated method to identify diffuse emission that is unrelated to the current star formation process).

We derive $\tau_{\text{dep}}$ from the total molecular gas mass, $M_{\text{mol}}$, as is commonly done. If the molecular gas that is not in our cloud catalog is indeed in a diffuse phase that is not (immediately) participating in the star formation process, then the instantaneous depletion time for the clouds that we study will be shorter, $M_{\text{mol}}$, and thus $\tau_{\text{dep}}$, would be scaled down on average by a factor $f_{\text{dep}} \sim 0.3$. $\epsilon_{\text{dyn}}$ would be scaled upwards by a factor of $\sim 3$. Applying such a correction would approximately conserve the difference between low- and high-$\alpha_{\text{vir}}$ targets, because the relative shift between the two is a factor of $\lesssim 1.5$, so that our main conclusions remain unchanged. Such a correction might help reconcile our observations with some of the Milky Way work, but without understanding the interaction of GMCs and diffuse gas, the physical meaning of such a correction is unclear.
3.3. Comparison to Theoretical Models

Figure 2 shows the “single free-fall time” version of the KM05, PN11, P12, and HC11 models (introduced in Section 1.2) as dashed–dotted curves. Overall, the models have the tendency to predict $\epsilon_{\text{dyn}}$ larger than what we observe, sometimes overpredicting the observations by $\sim 1$–2 orders of magnitude. The discrepancy is largest for clouds in high-pressure environments with small $\alpha_{\text{vir}} \approx 1$–2 (i.e., the inner, gas-rich disks of galaxies) that have $\epsilon_{\text{dyn}} \approx 0.05\%$–0.5%, which is $\sim 2$ dex below the model predictions. For clouds in low-pressure environments—for which we already noted the finding of an anticorrelation between $\epsilon_{\text{dyn}}$ and $\alpha_{\text{vir}}$—the KM05 (see also footnote 7) and P12 models are in good agreement with our observations, whereas the PN11 and HC11 models predict a similar trend but with $\epsilon_{\text{dyn}}$ values that are $\sim 1$ dex higher than observed. What is apparent from Figure 2 is that none of the models can match all of our measurements, i.e., clouds in low- and high-pressure environments, by a single relationship.

Figure 3 investigates whether the additional model parameters ($M_\text{vir}$, $b$, and $\beta$) can be adjusted to improve the agreement with our observations (as shown in Figure 2). In each panel, we show the SFE per dynamical time, $\epsilon_{\text{dyn}}$, predicted by the KM05, PN11, and HC11 models as a function of the virial parameter, $\alpha_{\text{vir}}$. In each panel, we vary one of the three additional model parameters. The left column shows the model predictions for the single free-fall time formulation and the right column for the multi-free-fall time ones. From top to bottom, the varied model parameters are the turbulent Mach number ($M_\text{vir}$), the turbulence-driving parameter $b$, and the plasma $\beta$ describing the strength of the turbulent magnetic field ($\beta \to \infty$ for negligible magnetic fields). While varying one of these parameters, we keep the other two fixed at their default values; the considered ranges are $M_\text{vir} = 2$–50, $b = 0.3$–1.0, and $\beta = 0.1$–$10^4$, which represent the maximum plausible ranges for the galactic environments studied here (e.g., Federrath & Klessen 2012; Padoan et al. 2014).

We find that the turbulence-regulated models of star formation (with the exception of the HC11 model) struggle to match the observed systematic variations in SFE per dynamical time for any plausible range in their four model parameters ($\alpha_{\text{vir}}$, $M_\text{vir}$, $b$, or $\beta$) without an ad hoc adjustment of the overall normalization of the models. We can rule out that variations in $\alpha_{\text{vir}}$ or $\beta$ alone can reproduce the spread in the observed $\epsilon_{\text{dyn}}$ values. Variations in $M_\text{vir}$ and $b$ cover a (somewhat) larger range of $\epsilon_{\text{dyn}}$ but still smaller than the observed range in $\epsilon_{\text{dyn}}$. Thus, simultaneous variations in several parameters would be needed for the models to match the observations. This would require gas-rich, inner galaxy disks (commonly having $\alpha_{\text{vir}} \approx 1$–2) to have low Mach numbers ($M_\text{vir} \sim 2$–5), predominantly solenoidal turbulence driving ($b \sim 0.3$–0.4), or non-negligible turbulent magnetic pressure ($\beta < 10$). On the other hand, gas-poor, outer galaxy disks (having $\alpha_{\text{vir}} \approx 3$–20) would require high Mach numbers ($M_\text{vir} \sim 10$–50), mostly compressive turbulence driving ($b \sim 0.5$–0.8), and negligible turbulent magnetic pressure ($\beta > 100$). These parameter ranges represent predictions for future observations, under the assumption that current turbulent star formation theories accurately describe the SFRs in the environments considered.

Each of the above conditions must be satisfied in order to reconcile the turbulent cloud models with our observations. Encouragingly, it is reasonable to expect an increased degree of solenoidal turbulence driving (due to shear; e.g., Krumholz & Krumholz 2015; Kruijssen et al. 2019a) or elevated magnetic pressures (e.g., Pillai et al. 2015; Federrath et al. 2016) toward galactic centers. However, the requirement of a low Mach number in the inner disks of galaxies stands against flat or falling radial velocity dispersion profiles observed in nearby galaxies (e.g., Wilson et al. 2011; Caldú-Primo et al. 2013; Mogotsi et al. 2016; Sun et al. 2018) or simple disk-center decompositions carried out for the Milky Way (e.g., Oka et al. 2001; Shetty et al. 2012; Kruijssen & Longmore 2013). This means that the data points at low $\alpha_{\text{vir}}$ and low $\epsilon_{\text{dyn}}$ (bottom left in Figure 3) are out of reach of the considered models.

Overall, we conclude that if one searched for a description of the SFE per free-fall time that works in all environments found in nearby galaxies, then the simplest model of a constant $\epsilon_{\text{dyn}} \approx 1\%$ matches the observations at least as well as any of the more sophisticated models that we tested. If one considers only low-pressure environments—such as the solar neighborhood—then the turbulence-regulated models can provide a superior description of the observations with respect of a constant $\epsilon_{\text{dyn}}$ as long as the model’s fudge factors (in particular the overall normalization) are appropriately adjusted (this requirement has also been pointed out by Leroy et al. 2017a; Ochsendorf et al. 2017). However, in the vein of Barnes et al. (2017), we have to conclude that the falsification of these star formation theories is currently obstructed by the lack of consensus on the values of their free parameters.

In line with several recent studies, our observations show that current models of turbulence-regulated star formation—based on idealized assumptions of cloud-scale density structure and turbulence, and assuming a stationary SFR—do not fully capture observations across a diverse range of galactic and extragalactic star-forming environments (Lee et al. 2016; Barnes et al. 2017; Leroy et al. 2017a; Ochsendorf et al. 2017). The discrepancy may reflect observational limitations in constraining the relevant physical parameters (e.g., uncertain mass-to-light conversion and beam-diluted measurements); however, it could also be of physical origin in that cloud-scale turbulent properties insufficiently reflect the dynamic “boundary” conditions of star-forming molecular clouds and that additional large-scale processes are relevant (e.g., implying environmental changes in the sonic and Alfvén Mach number and the nature of turbulence driving). Moreover, it may imply the relevance of other parameters (e.g., the cloud lifetime or feedback efficiency) that have not yet been considered by analytic theories.

4. Outlook

Within the next years, it will become possible to study the relationship between galactic structure, ISM properties, and star formation in unprecedented detail. With ALMA, we can now map the molecular gas (traced by CO emission) at cloud-scale resolution across entire galaxies (and samples thereof). Performing homogeneous analyses of such data with refined methodology (e.g., Leroy et al. 2016) can lead to accurate determinations of ISM properties such as the virial state of gas (Sun et al. 2018). Comparison of these properties in smaller...
Figure 3. Star formation efficiency, $\epsilon_{\text{SFH}}$, as a function of the observed virial parameter, $\alpha_{\text{vir}}$, and the related ratio of the free-fall and turbulent crossing time, $\tau_{\text{ff}}/\tau_{\text{cross}}$ (top x-axis; same data as in Figure 2) for the single free-fall (left panels) and multi free-fall (right panels) models. The three panels from top to bottom show how the models vary within (plausible) ranges of the unconstrained model parameters: sonic Mach number, $M$; turbulence-driving parameter, $b$; and the plasma $\beta$ parameter describing the strength of the turbulent magnetic field ($\beta \to \infty$ implies no magnetic fields). In each panel, we vary one of the three parameters while keeping the other two fixed at their default values (see text).
(kiloparsec-scale) patches of galaxies allows a more accurate description of (their correlation with) the local galactic host environment. Additionally, observations with VLT/MUSE and JWST can trace early (massive) star formation, which enables studies of individual star-forming clouds as routinely performed in the Milky Way. Observations of higher critical density tracers (e.g., HCN) provide information on the gas density distribution. While cloud-scale mapping of dense gas tracers remains a challenge even with ALMA, coarser (kiloparsec-scale) observations provide valuable insight, too (e.g., Usero et al. 2015; Bigiel et al. 2016; Gallagher et al. 2018), and can be further refined by modeling of the unresolved ISM structure (Leroy et al. 2017b). All of these steps are goals of the PHANGS (see footnote) collaboration.

In addition, observations that zoom in on the clouds in both H1 and CO tracers are desired. Especially for diffuse clouds dominated by ambient pressure, it is of interest to know their internal structure, look for gravitational bound cores, and search for H1 shielding envelopes around CO-bright cores. A first such assessment has been possible using parsec-scale CO observations with ALMA of star-forming regions in the Local Group dwarf galaxy NGC 6822 (Schruba et al. 2017). Moreover, we want to know whether the CO is a continuous part of a H1 turbulent cascade or whether the chemical transition coincides with a transition in energy balance.

To further expand and test the model of turbulence-regulated star formation, it is desirable that the model fudge factors, which so far have been constrained with idealized, turbulent box simulations and vary significantly between different calibrations (e.g., Federrath & Klessen 2012), are calibrated with galaxy-scale simulations. Moreover, we require predictions along the evolutionary tracks of star-forming clouds to interpret the scatter in cloud-scale resolved observations. Direct observational constraints on the evolutionary timeline of molecular clouds and the efficiency of stellar feedback are currently being derived (e.g., Kruitjes & Longmore 2014; Kruitjes et al. 2018, 2019b; Chevance et al. 2019). Additionally, obtaining Mach number measurements across a wide dynamical range of spatial scales (i.e., through the size–line–width relation) will provide critical input for testing the role of turbulent energy driving and dissipation in turbulent star formation models. This will require high dynamic range ALMA observations. Finally, these different aspects need to be brought together to form a self-consistent theory that connects both galactic and cloud-scale ISM structure and star formation, with first progress underway (e.g., Ostriker et al. 2010; Semenov et al. 2016; Krumholz et al. 2018, and others).

5. Summary

We built the largest compilation of measured molecular cloud properties and their galactic host environments, covering the Milky Way and seven nearby galaxies. Using mass-weighted mean molecular cloud properties for entire galaxies or distinct subregions therein, we study (a) the environmental dependence of the dynamical state of molecular clouds and (b) the impact of the clouds’ dynamical state on the global star formation activity, which we use to test analytic models of turbulence-regulated star formation. Our main findings are as follows:

1. Molecular clouds are in ambient pressure-balanced virial equilibrium. In gas-rich, molecular-dominated, high-pressure regions of galaxies, clouds are near virialization considering only their self-gravity ($\alpha_{\text{vir}} \approx 1–2$). Clouds in lower surface density, atomic-gas-dominated, low-pressure environments have $P_{\text{int}} \sim P_{\text{ext}}$ (resulting in $\alpha_{\text{vir}} \approx 3–20$) and are thus pressure-confined.

2. The SFE per free-fall time is low ($\epsilon_{\text{ff}} \approx 0.1\%–1\%$), has significant (1–2 dex) scatter, and systematically varies with $\alpha_{\text{vir}}$ and host galactic properties. For low-pressure, atomic-dominated regions, we find a common trend (anticorrelation) between $\epsilon_{\text{ff}}$ and $\alpha_{\text{vir}}$.

3. Models of turbulence-regulated star formation can provide a good match to the observations when considering only low-pressure, atomic-dominated regions and allowing for an ad hoc adjustment of the overall normalization. The low observed $\epsilon_{\text{ff}}$ for clouds in high-pressure, molecular-dominated regions is not well reproduced by these models even when considering the maximum plausible range in the additional model parameters (Mach number, turbulence driving, and magnetic field strength) that could not be constrained by the available data. This suggests the importance of additional physical parameters not yet considered by these models.

We highlight that studies linking cloud-scale ISM properties, star formation, and their galactic environment are in their infancy. Within the next years, we expect many more insights from multiwavelength, cloud-scale imaging surveys of nearby galaxies with ALMA, VLT/MUSE, and JWST. At the same time, the expansion of numerical simulations and analytic modeling to multiscale models will be indispensable for interpreting the observations and building a self-consistent theory of galactic and cloud-scale ISM properties and star formation.

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