A folded-sandwich polarization-entangled two-color photon pair source with large tuning capability for applications in hybrid quantum systems

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Abstract We demonstrate a two-color entangled photon pair source which can be adapted easily to a wide range of wavelength combinations. A Fresnel rhomb as a geometrical quarter-wave plate and a versatile combination of compensation crystals are key components of the source. Entanglement of two photons at the Cs D1 line (894.3 nm) and at the telecom O-band (1313.1 nm) with a fidelity of $F = 0.753 \pm 0.021$ is demonstrated, and improvements of the setup are discussed.

1 Introduction

In recent years, there has been an increasing effort to realize and study quantum hybrid systems. These consist of two dissimilar systems—often at different wavelengths—which are in a joint quantum state. Aside from the fundamental insight gained from studying such a peculiar, perhaps multi-particle entangled state, there are also immediate applications in quantum information processing. Entanglement of a stationary and flying qubit, i.e., an electronic state with a long coherence time and a photon, respectively, represents a coherent quantum interface. Such interfaces are mandatory components of a quantum repeater [1], where entanglement has to be established between distant nodes. Experimental realizations demonstrated entanglement between a photon and a stationary state in atoms [2], ions [3], semiconductor quantum dots [4], color defect centers [5] and even superconducting qubits [6]. A Bell measurement on two photons of each of two such states would then immediately establish entanglement between two stationary, possibly dissimilar states [7, 8]. However, two dissimilar systems may emit light at vastly different wavelengths. It is not possible to entangle such systems with different transition energies via a Bell state measurement. One possible solution of this problem is to use a two-color pair of entangled photons, which are color-matched to these two different transitions as shown in Fig. 1a. The two-color photon pair source mediates entanglement between two dissimilar wavelengths. In the same manner, it can convert the wavelength of flying qubits as shown in Fig. 1b. This is especially helpful if entanglement should be established over long distances, e.g., via optical fibers in the telecom band. The key building block in these two applications is a source of non-degenerate entangled photons. Especially when working with systems whose wavelengths are hundreds of nanometers apart, such a source has to generate highly non-degenerate photons. In contrast to previous highly non-degenerate sources [9], our source introduces wavelength-insensitive components and is thus in principle widely tunable. This is another important requirement when working with a variety of different systems in hybrid systems, in particular with systems that may vary in time or from experiment to experiment.

Up to now, the brightest and most practical sources of entangled photon pairs rely on spontaneous parametric down-conversion in nonlinear crystals [10]. With appropriate phase matching, two-color sources with photons at different wavelengths can be realized [9, 11, 12]. For subsequent fiber coupling, collinear down-conversion schemes are most convenient. Furthermore, the collinear alignment enables further integration and can be used in a monolithic design [12].
There are different possible collinear arrangements. Figure 2 shows the two-crystal Sagnac [9], the crossed-crystal [13] and the folded-sandwich configuration [14].

The rotation of the second crystal in the crossed-crystal configuration (Fig. 2b) can be replaced by a half-wave plate. Replacing the half-wave plate and the second crystal by a quarter-wave plate and a mirror yields the folded-sandwich scheme (Fig. 2c). Using only a single nonlinear crystal makes it considerably easier to avoid the leakage of which-crystal information. The folded-sandwich and the crossed-crystal configuration include a compensation crystal, which compensates the additional dispersion, whereas this is not needed in a two-crystal Sagnac configuration.

Together with the pump, any two-color entangled photon source involves three fields of widely different wavelengths. This imposes strong constraints on dispersion compensation. In particular, a source for generating entanglement in quantum hybrid systems should be easy to align, intrinsically stable and tunable in order to account for various transition frequencies. The Sagnac configuration requires a special three-color beam splitter and is very difficult to align [14]. The crossed-crystal configuration lacks the phase stability of the Sagnac configuration. Therefore, it is desirable to use the simpler folded-sandwich configuration. In this paper we show for the first time how the folded-sandwich can be used to generate highly non-degenerate photons. To this end, we slightly modify the folded-sandwich configuration. In contrast to previous work, we employ geometrical, i.e., wavelength-independent, polarization manipulation.

Here, we target for a two-color entangled photon source at $\lambda_3 = 894.3$ nm and $\lambda_i = 1313.1$ nm. These two wavelengths correspond to the Cs D1 line and the telecom O-band, respectively. The former has been chosen on the one hand as a convenient standard atomic transition. On the other hand, it is also accessible with excitonic transitions in InGaAs quantum dots [15]. The source is thus applicable for quantum hybrid systems [16, 17] involving atomic species, semiconductor quantum dots or molecules as well as long-distance transfer via optical fibers. Here we aim on long-distance transfer of qubits from quantum dots.
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\[ n_i = n_e - \sqrt{n_s^2 - (n_e - n_i)^2} \]

The crystal temperature is controlled via a crystal oven (not shown). The Fresnel rhomb acts as a geometrical quarter-wave plate. The concave mirror (CM) reflects the light back onto the Fresnel rhomb and the nonlinear crystal a second time. Again, this accumulated which-crystal information would diminish the entanglement.

\[ \phi(\lambda_s, \lambda_i, T) = \left( \frac{n_0(\lambda_s, T)}{\lambda_s} + \frac{n_o(\lambda_i, T)}{\lambda_i} \right) L_{\text{crystal}} \]

\[ + \left( \frac{n_0(\lambda_s)}{\lambda_s} + \frac{n_i(\lambda_i)}{\lambda_i} \right) 2L_{\text{rhomb}}, \]

where \( n_s \) is the refractive index of the nonlinear crystal (YVO4). In our experiment, we chose undoped YVO4 as a birefringent compensation crystal. A crystal of length \( L \) adds a phase of

\[ \phi(\lambda_s, \lambda_i, T) = \left( \frac{\tilde{n}_(\lambda_s, T)}{\lambda_s} + \frac{\tilde{n}_e(\lambda_i, T)}{\lambda_i} \right) L, \]

\[ - \frac{\tilde{n}_e(\lambda_s, T)}{\lambda_s} - \frac{\tilde{n}_e(\lambda_i, T)}{\lambda_i} \]

where \( \tilde{n}_{0/e} \) is the refractive index of the ordinary and extraordinary axis of YVO4.

The flat phase condition for optimum compensation with the two different photon wavelengths \( \lambda_s \) and \( \lambda_i \) reads:

\[ \frac{d}{d\lambda} \left( \phi + \tilde{\phi} \right) \bigg|_{\lambda_s, \lambda_i} = 0. \]

\[ \phi(\lambda_s, \lambda_i, T) \]

\[ \phi(\lambda_s, \lambda_i, T) = \left( \frac{n_0(\lambda_s, T)}{\lambda_s} + \frac{n_o(\lambda_i, T)}{\lambda_i} \right) L_{\text{crystal}} \]

\[ + \left( \frac{n_0(\lambda_s)}{\lambda_s} + \frac{n_i(\lambda_i)}{\lambda_i} \right) 2L_{\text{rhomb}}, \]
Table 1  Reported refractive index difference $\Delta n = n_o - n_e$ of the ordinary and extraordinary axis of YVO$_4$ from different sources and the calculated corresponding length of compensation crystal for $\lambda_o = 894.3$ nm and $\lambda_i = 1313.1$ nm

| Source                                      | $\Delta n_o$ | $\Delta n_i$ | L (mm) |
|---------------------------------------------|--------------|--------------|--------|
| Manufacturer (Foctek) [19]                  | 0.211014     | 0.205271     | 138.7  |
| Zelmon et al. [20]                          | 0.211408     | 0.205448     | 154.0  |
| Sato et al. [21]                            | 0.211750     | 0.205685     | 172.0  |
| Handbook of optics [22]                     | 0.209959     | 0.204678     | 178.8  |

Fig. 4  Calculated phase $\phi + \tilde{\phi}$ as a function of the wavelength for two different lengths of the compensation crystal (constant offset subtracted). A flat phase is obtained for $L = 154$ mm (solid line) for the two target wavelengths $\lambda_o = 894.3$ nm and $\lambda_i = 1313.1$ nm (vertical lines). The plateaus of the flat phases are shifted considerably for $L = 153$ mm (dashed line). Based on refractive index data reported by Zelmon et al. [20].

There are different values for the birefringent properties of YVO$_4$ in the literature. Table 1 lists the refractive index difference of the ordinary and extraordinary axis of YVO$_4$ and the calculated length of a compensation crystal for the wavelengths $\lambda_o = 894.3$ nm and $\lambda_i = 1313.1$ nm for different sources. For the values that Zelmon et al. provide [20], Fig. 4 shows the calculated phase $\phi + \tilde{\phi}$ as a function of the wavelength for two different lengths of the compensation crystal. The two target wavelengths $\lambda_o = 894.3$ nm and $\lambda_i = 1313.1$ nm are plotted as vertical lines.

For $\pm 1$ mm crystal length, the two flat phase positions vary by $\pm 50$ nm. Thus with adding or removing additional few mm slabs of YVO$_4$, the total compensation can be tuned by several hundred nanometers. Each slab introduces losses. Therefore, it is convenient to use AR-coated and as few slabs as possible. In this experiment, the refractive indices had to be examined first; therefore, a flexible set of seven slabs was chosen, which reduced the transmission to 82.64%.

Finally, Fig. 5 demonstrates the tuning capability of our source. The crystal oven of the nonlinear crystal can be heated up to 160°C. The measured tuning range of the signal photon wavelength for the chosen 7 µm grating extends from 870 to 1100 nm; this is roughly 230 nm. The corresponding idler wavelength spans from 1124 to 1345 nm (not shown). The measurement was performed without compensation crystal.

3 Determining the optimal crystal length

The wave plates in each arm (after DM2 in Fig. 3) can be rotated such that photon coincidences in different bases can be measured. Both polarizers are fixed to horizontal polarization, such that in each arm the basis $|H\rangle$ is measured for a half-wave plate position of $\Theta_{\text{HWP}} = 0$. Rotating the half-wave plate to $\Theta_{\text{HWP}} = \pm 22.5^\circ$, the diagonal $|D\rangle$ and anti-diagonal $|A\rangle$ basis is measured, respectively. Adding a quarter-wave plate, the left $|L\rangle$ and right $|R\rangle$ basis can be measured. Each arm can be set to an individual polarization. For example, setting both arms to left-circular polarization is denoted $|L\rangle_{\text{signal}}|L\rangle_{\text{idler}} = |LL\rangle$ in the following.

The procedure to find the right compensation crystal relies on measuring polarization-sensitive coincidence counts as a function of the orientation of the half-wave plate $\Theta_{\text{HWP}}$ in one arm. Fig. 6 shows such measurements in different bases combinations. The measured curve can be fitted to a sine function, and the visibility can be derived (see next Section for details). Then, thin slabs of YVO$_4$ are added, until the visibility cannot be enhanced further. In this way, an optimum total length of the compensation crystal can be found.

Unfortunately, tuning by adding thin slabs of additional compensation crystals does not provide sufficient accuracy.
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Therefore, a fine tuning of the phase between 0 and \( \pi \) to generate a specific Bell state is necessary.

In order to do this, we changed the temperature of a 30 mm compensation crystal slab. Figure 7 shows the measured coincidence counts between signal and idler photons in the \(|AA\rangle\) basis as a function of the temperature of the compensation crystal. We find a phase shift of \( \pi \), i.e., between two different Bell states, for \( \sim 2.4 ^\circ \text{C} \) temperature difference.

For the wavelengths \( \lambda_s = 894.3 \text{ nm} \) and \( \lambda_i = 13.1 \text{ nm} \) we find a optimal total crystal length of \( L = 153 \text{ mm} \). The total length was composed of 7 slabs YVO\(_4\) of 2 cm length and one slab of 1 cm, 2 mm and 1 mm length. The total length is close to some of the reported data on the refractive index of YVO\(_4\) in the literature [20], even though they investigated 0.5 % Nd-doped YVO\(_4\). However, it deviates from the value reported by other studies [21], as well as from the manufacturer specification (Foectek Inc.) [19].

With the experimentally determined crystal parameters, it is in principle straightforward to estimate the compensation crystal length also for other pairs of wavelengths. Additional crystal slabs can be added or removed allowing for a wide tuning range.

4 Verifying entanglement

To quantify the degree of entanglement for optimized conditions, we measured the \( |\phi^+\rangle \) Bell-state fidelity \( F_{\phi^+} \) of the created state \( \rho \).

\[
F_{\phi^+} = \langle \phi^+ | \rho | \phi^+ \rangle. \tag{5}
\]

A fidelity \( F_{\phi^+} > \frac{1}{2} \) indicates entanglement [23]. In order to relate the fidelity to the coincidence probabilities, we use the two-photon polarization basis states \( |u_1\rangle = |HH\rangle, |u_2\rangle = |HV\rangle, |u_3\rangle = |VH\rangle, |u_4\rangle = |VV\rangle \). After expanding \( \rho \) in this basis and using

\[
|\phi^+\rangle = \frac{1}{\sqrt{2}} (|u_1\rangle + |u_4\rangle), \tag{6}
\]

\[
\text{Fig. 6 Measured coincidence counts as a function of the orientation of the half-wave plate in different bases combinations. The dashed and solid lines are fits to sine functions. The resulting visibilities } v_j \text{ from Eq. (15) are indicated.}
\]

\[
\text{Fig. 7 Measured coincidence counts in the } |AA\rangle \text{ basis (both polarizers anti-diagonal) as a function of the temperature of a 30 mm compensation crystal slab. The total crystal length is 153 mm.}
\]
we get
\[ F_{\phi^+} = \sum_{k=1}^{4} \rho_{kl} \langle \phi^+ | u_k \rangle \langle u_l | \phi^+ \rangle \]
\[ = \frac{1}{2} (\rho_{11} + \rho_{14} + \rho_{41} + \rho_{44}), \]  
where \( \rho_{kl} = \langle u_k | \rho | u_l \rangle \). The diagonal elements \( \rho_{11} \) and \( \rho_{44} \) are the probabilities \( P_H \) and \( P_V \) of finding a photon pair in the states \( |HH\rangle \) and \( |VV\rangle \), respectively. The off-diagonal elements can be expressed with the help of the diagonal and circular basis,
\[ P_D + P_A = \langle DD | \rho | DD \rangle + \langle AA | \rho | AA \rangle \]
\[ = \frac{1}{2} (1 + \rho_{14} + \rho_{41} + \rho_{23} + \rho_{32}), \]
\[ P_R + P_L = \frac{1}{2} (1 - \rho_{14} - \rho_{41} + \rho_{23} + \rho_{32}) \]
and thus
\[ P_D + P_A - (P_R + P_L) = \rho_{14} + \rho_{41}. \]
We therefore obtain the fidelity as a function of the probabilities in the three different bases,
\[ F_{\phi^+} = \frac{1}{2} [P_D + P_A - (P_R + P_L) + P_H + P_V]. \]
These probabilities can be measured as they are connected to the coincidence count rates \( N_i \),
\[ P_i = \frac{N_{ii} + N_{ij} + N_{ji} + N_{jj}}{N_{tot}}, \]
where \( i \) refers to the one-photon polarization state orthogonal to \( j \), that is \( i/j = H/V, D/A, \) or \( L/R \). After introducing
\[ V_{ij} = \frac{N_{ii} + N_{ij} - (N_{ij} + N_{ji})}{N_{ii} + N_{ij} + N_{ji} + N_{jj}} = \frac{2(N_{ii} + N_{ij})}{N_{tot}} - 1 \]
Equation (11) yields the alternative representation [14]
\[ F_{\phi^+} = \frac{1}{4} (1 + V_{HV} + V_{DA} - V_{LR}). \]
To determine the fidelity, we measured the visibilities
\[ v_i = \frac{N_{ii} - N_{ij}}{N_{ii} + N_{ij}} = \frac{A_i}{C_i} \]
in the three different bases, as shown in Fig. 6. In the measurement, the basis in one arm is fixed, while the basis in the other arm is rotated between \( i \) and its orthogonal counter part \( j \). The visibilities are then fitted with a sine function \( A_i \sin(4\phi_{1WP} + \text{const.}) + C_i \). Since \( C_i = (N_{ii} + N_{ij})/2 \) and \( A_i = (N_{ii} - N_{ij})/2 \), we have
\[ V_{ij} = \frac{A_i + A_j}{C_i + C_j}. \]
With this, we find a fidelity of \( F_{\phi^+} = 0.753 \pm 0.021 \) for our source at a photon pair generation rate of 5.8 Mcps/mW and spectral linewidths of 560 GHz, which corresponds to 1.5 and 3.3 nm at \( \lambda_H = 894.3 \) nm and \( \lambda_D = 1313.1 \) nm, respectively. In order to match the bandwidth of the photons to stationary quantum systems, additional spectral filtering is required. External volume Bragg gratings and etalons have been used for this purpose [24, 25] starting with very similar bandwidths [25] as in our source. It is apparent that the initial spectral brightness has to be as large as possible in order to provide a reasonable photon pair rate after the filters. These values were calculated from a count rate of 215 kcts/s at 370 \( \mu \)W and a detection efficiency of 0.1.

The error for the fidelity was calculated from the correlated errors of the visibilities (shown in Fig. 6). The uncertainties of the individual data points that stem from accidental coincident are negligibly small. Therefore, the error was estimated from the fit itself. The differences in the visibilities of orthogonal bases are due to a variety of reasons, such as the displacement differences in beam waists of H and V beam and a non-perpendicular incident on one of the compensation crystals causing wavelength-dependent diffraction. The limited visibility can be explained by temperature fluctuations of the compensation crystals. The total length of the compensation crystal is \( L = 153 \) mm, but only a small fraction (3 cm) of the crystal is temperature-stabilized inside the crystal oven. Small changes in temperature modify the optical path lengths of extraordinarily and ordinarily polarized photons and lead to a fluctuating phase. For our configuration, the temperature fluctuations at the compensation crystals of \( \pm 1 \) K are the strongest factor that reduces the fidelity (see also [14]). Temperature control and stabilization will also allow for better adjustment of the refractive indices, which in turn will enhance the visibility. With an improved temperature, stabilization of 0.1 K and a thermally isolated housing of the compensation crystals fidelities above 95 \% should be possible (as estimated in [14]).

5 Conclusion
We demonstrated a novel folded-sandwich scheme for the generation of two-color entangled photons which uses a Fresnel rhomb as a geometrical quarter-wave plate. By this, all optical components are more easily adapted to wide combinations of wavelengths. For example, no three-color beam splitters as in a Sagnac configuration are required. Adjusting the compensation crystal length offers a tuning
capability over more than 100 nm. Our source is a viable tool to provide highly non-degenerate entangled photons for quantum hybrid systems, in particular when solid-state emitters with an a priori unpredictable transition frequency are involved.

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