Electronic, magnetic, optical and thermoelectric properties of co-doped Sn$_{1-2x}$Mn$_x$A$_x$O$_2$ (A = Mo, Tc): a first principles insight

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The electronic, magnetic, optical and thermoelectric (TE) properties of Sn$_{1-2x}$Mn$_x$A$_x$O$_2$ (A = Mo/Tc) have been examined using density functional theory (DFT) based on the FP-LAPW approach. The results suggested that all the doped compounds show a half-metallic ferromagnetic property with a 100% spin polarization at the Fermi level within GGA and mBJ. Moreover, doping SnO$_2$ with double impurities reduces the bandgap. The reduced bandgaps are the result of impurity states which arise due to the Mn and Mo/Tc doping, leading to the shifts of the minima of the conduction band towards the Fermi energy caused by the hybridization between different transition metals 3d and O-2p states. The (Mn, Mo) co-doped SnO$_2$ system exhibits a ferromagnetic ground state which may be explained by the Zener double exchange mechanism. While the (Mn, Tc) co-doped SnO$_2$ system is p–d hybridization. Therefore, the role of this study is to illustrate the fact that half-metallic ferromagnetic material is a good absorber of sunlight (visible range) and couples to give a combined effect of spintronics with optronics. Our analysis shows that Sn$_{1-2x}$Mn$_x$MoO$_2$ and Sn$_{1-2x}$Mn$_x$TeO$_2$ are more capable of absorbing sunlight in the visible range compared to pristine SnO$_2$. In addition, we report a significant result for the thermoelectric efficiency $ZT$ of ~0.114 and ~0.11 for Sn$_{1-2x}$Mn$_x$MoO$_2$ and Sn$_{1-2x}$Mn$_x$TeO$_2$, respectively. Thus, the coupling of these magnetic, optical, and thermoelectric properties in (Mn, A = Mo or Tc) co-doped SnO$_2$ can predict that these materials are suitable for optoelectronic and thermoelectric systems.

1 Introduction

Transparent conducting oxides (TCOs) are materials that exhibit good optical transparency in the visible range, high electrical conductivity, and good carrier density. For photovoltaic conversion, a few micrometers thick film made of direct bandgap materials like II–VI or III–V compound semiconductors is sufficient. One of these materials, tin oxide (SnO$_2$), is characterized as having a large direct bandgap (3.6 eV) at room temperature. SnO$_2$ currently occupies a prominent place because of the wide availability of the raw material and its non-toxicity. It is a semiconductor material possessing interesting physical properties which place it among the most promising in various fields such as optoelectronic devices, and solar cells and could be a good thermoelectric material. Interestingly, doping SnO$_2$ with transition metal elements (Mo, Cr, Mn, Rh, Co, Al, and Fe) induces a spin functionality which creates an opportunity in the field of electron spin that is being widely investigated today. This kind of material creates a new class of materials called diluted magnetic semiconductors (DMSs). Ferromagnetic behaviour has been reported in co-doped SnO$_2$ with a large magnetic moment of ~7.0 $\mu_B$ at room temperature. Ogale et al. reported that 5% Co doped SnO$_2$ is a high-temperature ferromagnet with $T_c = 650$ K and a giant magnetic moment. Also, Okabayashi et al. researched the ferromagnetic (FM) properties of samples and revealed that (Fe, Mn) co-doped SnO$_2$ preserves ferromagnetism. This study provides ample data on high optical absorption in the visible range and high electrical conductivity accomplished by impurity doping. Lin et al. reported the effects of (Mn, Co) co-doped SnO$_2$ on optical characteristics. Their results show that the absorption efficiency of (Mn, Co) co-doped SnO$_2$ in visible light
was greatly improved. Spintronics coupled with optoelectronics has mostly remained an unexplored field despite the various research studies which have been carried out on this topic. A ferromagnetic DMS has yet to be used in the fabrication of solar cells, although it could be a vital material in future solar cell technology. SnO₂ co-doped with rare earth elements (Eu, Gd) demonstrates that this ferromagnetic alloy can absorb up to 96% in the visible light range and it can convert heat energy into electricity efficiently at room temperature.\(^{17}\) The efficiency of a thermoelectric material in converting heat into electrical energy is defined by the figure of merit, where $S$ is the Seebeck coefficient, $\sigma$ the electrical conductivity, $K$ the total thermal conductivity and $T$ the absolute temperature.\(^{18\text{-}26}\) The charge carrier concentration and mobility control both the Seebeck coefficient and the electrical conductivity. Additionally, some earlier studies showed that even magnetic materials give a significant good thermoelectric response, eventually improving the Seebeck coefficient such as: demonstration of magnon drag at relatively high temperatures,\(^{27}\) paramagnon drag,\(^{28\text{-}30}\) spin fluctuation,\(^{31}\) spin entropy.\(^{32}\) Chang et al.\(^{33}\) showed that doping RuS₂ with Mn alters the electronic structure, creating a ferromagnetic (FM) conductor with good thermoelectric properties. Also, Yousuf et al. discovered the half-metallic ferromagnetic character of Zr₂NiZ (Z = Al, Ga) Heusler alloys, along with their effective thermoelectric coefficients, which points to the possibility of their use in the development of spintronic devices and improving thermoelectric materials.\(^{34}\) The purpose of this work is to understand the properties of this ferromagnetic DMS under sunlight, particularly in the visible region, and how it might contribute to photovoltaic applications in a solar cell. As a result, we have examined the electronic, magnetic, optical, and thermoelectric properties of SnO₂ rutile doped with double impurities (Mn, A = Mo/Tc) using spin-polarized first-principles simulations. We have employed density functional theory (DFT) to perform our calculations, using the generalized gradient approximation (GGA-PBE)\(^{35\text{-}36}\) and the Tran–Blaha modified Becke–Johnson exchange potential approximation (TB-mBJ)\(^{37\text{-}38}\) as implemented in WIEN2K Code.\(^{39\text{-}40}\) The details of our computational strategy are described in Section 2 of this work. Section 3 includes our findings. Finally, Section 4 concludes the results.

2 Computational details

Tin dioxide adopts a rutile-type quadratic lattice with a space group $P4_3/mmm$. The parameters of the crystal lattice are as follows: $a = b = 4.74$ Å and $c = 3.18$ Å.\(^{41}\) The unit cell contains six atoms, four oxygen atoms and two tin atoms. Each tin atom is in the middle of a cage formed by a regular octahedron of six oxygen atoms, while each oxygen atom is surrounded by three tin atoms located at the vertices of an isosceles triangle. The oxygen is in position $4f$ given by $[u, u, 0]$, $[1 - u, 1 - u, 0]$, $[u + 1/2, 1/2 - u, 1/2]$, $[1/2 - u, u + 1/2, 1/2]$ with $u = 0.306$. Tin occupies position $2a$, $[0, 0, 0]$, $[1/2, 1/2, 1/2]$. In this work, the total calculations are obtained from \textit{ab initio} calculations based on density functional theory (DFT) adopted by the full-potential linearized augmented plane wave (FP-LAPW) method. The cutoff parameter is set to $R_{MT} \times K_{max} = 7.5$, where $K_{max}$ is the most valuable of the reciprocal lattice vectors in the plane wave expansion and $R_{MT}$ is the smallest atomic sphere radii of most atomic spheres. Here the MT radii are chosen to be $R = 1.76$ au. To insert the double-impurities a supercell of $[2 \times 2 \times 2]$ mesh was created [Sn₁₆O₃₂ supercell, see Fig. 1(a)]. We have utilized a self-consistent criterion of the total energy with an accuracy of $10^{-6}$ Ry and charge difference $\Delta Q = 10^{-6}$ between two successive iterations, considering the force equal to 0.1 mRy per au. An energy of $\sim 6.5$ Ry is utilized to separate the core states from the valence states. We have used a grid of 8813 $k$ points and 557 points (Sn₁₁₈MnAlO₃₂ supercell, with A = Mn/Tc) in the first Brillouin zone.\(^{42}\) In the supercell, the co-doped systems are developed by replacing two Sn atoms by Mn and A (M = Mo/Tc) atoms relating to concentration ratios of $x = 0.0625$ in Sn₁₋₂ₓMnₓAlO₂ [see Fig. 1(b and c)]. To determine the most stable magnetic state, both ferromagnetic (FM) and antiferromagnetic (AFM) states are determined. The total energy difference $\Delta E = E_{AFM} - E_{FM}$\(^{43}\) determines the stabilization of the magnetic

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**Fig. 1** $2 \times 2 \times 2$ supercell structures of (a) SnO₂, (b) Sn₁₋₂ₓMnₓMoₓO₂ and (c) Sn₁₋₂ₓMnₓTcₓO₂.
phase in the DMS. If the value is positive, the FM state is steady and stable but if the value is negative the AFM is steadily stable.

3 Results and discussion

3.1 Structural properties

The pristine and doped structures (SnO₂, Sn₁₋₂ₓMnₓMoₓO₂ and Sn₁₋₂ₓMnₓTcₓO₂) were optimized by the volume optimization method. To obtain the most stable structure with minimum ground state energy, we performed the curve fitting of the energy-vs.-volume data within the Murnaghan equation of state as:

\[
E(V) = E_0 + \frac{9V_0B_0}{16}
\left[\left(\frac{V_0}{V}\right)^{2/3} - 1\right]^3 B'_0
+ \left(\frac{V_0}{V}\right)^{2/3} - 1\right]^2 \left[6 - 4\left(\frac{V_0}{V}\right)^{2/3}\right]
\]  

(1)

where \(E_0\) is the equilibrium energy, \(V_0\) the original volume, \(V\) the obtained volume change, \(B\) is the bulk modulus and \(B'\) its first order pressure derivative. The smooth curves of energy-vs.-volume are obtained by fitting the data in the Murnaghan equation of state for the pristine and co-doped systems as shown in Fig. 2. The optimized lattice parameters are presented in Table 1 and are compared with the previous available data. For further analysis of structural stability of the doped and undoped materials we have calculated the formation energy \(E_{\text{for}}\) by using eqn (2):

\[
E_{\text{for}} = E_{\text{tot}} - \sum x E_x
\]  

(2)

where \(E_{\text{tot}}\) is the ground state total energy of the system, \(x\) is the number of individual components, \(E_x\) is the energy of an individual component in its bulk form. The calculated \(E_{\text{for}}\) for SnO₂, Sn₁₋₂ₓMnₓMoₓO₂ and Sn₁₋₂ₓMnₓTcₓO₂ are −2.42 eV per atom, −1.57 eV per atom and −1.54 eV per atom, respectively. The negative values of \(E_{\text{for}}\) indicate the stability of our systems.

3.2 Electronic properties

As we are aware, the electronic properties are not properly described by GGA-PBE. Most of the time the GGA bandgaps are underestimated. Therefore, herein we have presented the electronic properties results by calculating the total and partial densities of states (DOS) of pure and co-doped SnO₂ by using the TB-mBJ potential. Firstly, we have studied the electronic structure of pristine SnO₂ in the absence of any doping elements. The total and partial densities of states of pristine SnO₂ are shown in Fig. 3 by using the TB-mBJ approximation. The electron state density displays perfect symmetry among

![Figure 2](image-url)

Fig. 2 Volume vs. energy curve of (a) SnO₂ (2 × 2 × 2), (b) Sn₁₋₂ₓMnₓMoₓO₂ and (c) Sn₁₋₂ₓMnₓTcₓO₂.

![Figure 3](image-url)

Fig. 3 Total and partial density of states (DOS) of pristine SnO₂ obtained from TB-mBJ.

### Table 1 Optimized lattice constant (Å), bulk modulus (B) in GPa and its pressure derivative (\(B'\)) for bulk SnO₂ and Sn₁₋₂ₓMnₓAₓO₂ (A = Mo/Tc)

| System            | Lattice constant [our] | Bulk modulus (B) | Pressure derivative (\(B'\)) |
|-------------------|------------------------|------------------|------------------------------|
| SnO₂              | 4.737                  | 186.028          | 4.249                        |
| Ref. 7            | 4.767                  | —                | —                            |
| Ref. 41           | 4.74                   | 3.18             | —                            |
| Sn₁₋₂ₓMnₓMoₓO₂    | 13.57                  | 167.133          | 10.995                       |
| Sn₁₋₂ₓMnₓTcₓO₂    | 13.662                 | 177.672          | 0.454                        |
majority and minority spin states, which implies that SnO₂ is a non-magnetic material. The valence band is mainly formed by the O-2p orbitals and is full. While the conduction band is dominated by Sn-5s orbitals and is empty. The bandgaps calculated by using the TB-mBJ and GGA-PBE methods are 3.59 eV and 1.85 eV, respectively. In fact, the TB-mBJ approach gives a value for the bandgap closer to the experimental data.

Also, comparable results have been found in the previous theoretical calculations from PBE-GGA. The valence band has a width of 7.1 eV, which is in accordance with experimental and theoretical results.

To talk about the ferromagnetism in SnO₂ doped with dual impurities (Mn, A = Mo/Tc), we have calculated the electronic and magnetic properties of pure and co-doped SnO₂ corresponding to \(x = 0.0625\) in the first step. Fig. 4(a and b) show the total and partial densities of states (DOS) calculated by using the TB-mBJ approach. We observed that the total DOS is asymmetrical, which is a signature of magnetic behaviour. The half-metallic character appears clear in these figures where the Fermi level crosses the majority spin band, while the spin-down band is empty. The presence of energy levels near the upper part of the bandgap facilitates the excitation of electrons to the conduction band. Therefore, these calculations predict 100% spin polarization at the Fermi level. The majority spin bands at the Fermi level are mainly contributed by the Mo-d and Mn-d electrons, which suggests that the double impurities of Mn and Mo atoms do not result in the distortion of the nature of the host semiconductors.

The two possible magnetic configurations (FM and AFM) have been calculated and their energies compared. Our results indicate the stability of the ferromagnetic state in the Sn₁₋₂xMnₓMoₓO₂ compound with a strong half-metallic behaviour. Further investigating the origin of ferromagnetism in the system, the electronic structure calculations indicate a sufficiently large magnetic moment of 5 \(\mu_B\) for the cell. The high value of the total magnetic moment indicates a strong interaction between the double impurities. Also, the Mn and Mo atoms assume a significant part in the generation of the total magnetic moment and the partial magnetic moments contributed by Mn and Mo are 3.51 \(\mu_B\) and 0.81 \(\mu_B\) respectively. These values are compared with those obtained in single doped Sn₁₋₂xMnₓO₂ \(\left(m_{\text{Mn}} = 2.87 \mu_B\right)\) and Sn₁₋₂xMoₓO₂ \(\left(m_{\text{Mo}} = 1.31 \mu_B\right)\). The value of \(m_{\text{Mn}}\) is in close agreement with our previous result 2.87 \(\mu_B\).

The results for the total and partial magnetic moments are presented in Table 2. We could conclude that there is a charge transfer between the 4d electrons of the Mo atom and the 3d electrons of the Mn atom via the 2p orbitals of the O atom, to obtain an electronic configuration of d³ on [Mn³⁺ (3d³)] and d⁰ on [Mo⁰ (4d⁰)].
The total magnetic moment is from Mn (\( \mathbf{m} = 1.82 \mathbf{\mu}_B \)). In this manner, the mechanism responsible for ferromagnetic coupling is the Zener double exchange. As we have already discussed, the co-doping with Mn and Mo has brought about a drastic modification in the electronic and magnetic properties of SnO\(_2\). Furthermore, we have performed another co-doping by Mn and Tc with the concentration of \( x = 0.0625 \) by using TB-mBJ approximation. To inspect the stability of the magnetic phase in the (Mn, Tc) co-doped SnO\(_2\), we have calculated \( \Delta E \) and we have found that the AFM state is more stable than the FM state. The total and partial densities of states of Sn\(_{1-x}\)Mn\(_x\)Tc\(_x\)O\(_2\) are shown in Fig. 5. Total DOS has significantly asymmetry in the majority and minority spins, which comes from the Mn-3d, Tc-4d, and O-2p states. This suggests that the Mn-3d, Tc-4d and O-2p states have largely affected the induction of magnetic moment. Moreover, we could see that the spin-down state is empty, which is common in most of the DMS materials. Therefore, it is the \( p-d \) hybridization that is responsible for the magnetism in (Mn, Tc) co-doped SnO\(_2\). Consequently, the combination of all these characteristics in SnO\(_2\) co-doped with (Mn, Tc), such as free flow of charge carriers and half-metallic behaviour with the high total magnetic moment, resulted in a quality of materials suitable for spintronic device fabrication. To confirm our \textit{ab initio} findings, more experimentation will be required.

### 3.3 Optical properties

The optics of condensed media describe the interaction of an electromagnetic wave with the electrons of a solid. The linear response of electromagnetic radiation is described utilizing the dielectric function as:

\[
\varepsilon = \varepsilon_1 + i\varepsilon_2, \tag{3}
\]

where \( \varepsilon_1(\omega) \) and \( \varepsilon_2(\omega) \) are the real and imaginary parts of the dielectric function. \( \varepsilon_2(\omega) \) is inter-related to the electron transition between occupied and unoccupied states. The imaginary part defined the light absorption in the material and depends on the electronic transition; it is given by the following relation: \(^{10}\)

\[
\varepsilon_2(\omega) = \frac{n^2}{\varepsilon_0} \sum_{\mathbf{k}} \left| \mathbf{p} \right|^2 \left( f(\mathbf{k}) - f(\mathbf{k} + \mathbf{q}) \right) \left\{ 1 - f(\mathbf{k}) \right\} \Delta (E_{\mathbf{k}\mathbf{q}} - E_{\mathbf{k}+\mathbf{q}}) \tag{4}
\]

where \( \mathbf{p} \) is the momentum operator, \( f(\mathbf{k}) \) is the eigen-function of the eigenvalue, and \( f(\mathbf{k}) \) is the Fermi distribution function. The real part of the dielectric function \( \varepsilon_1(\omega) \) is derived from the imaginary part \( \varepsilon_2(\omega) \) using the Kramers-Kronig relation: \(^{19}\)

\[
\varepsilon_1(\omega) = 1 + \frac{2}{\pi} \int_0^\infty \frac{\varepsilon_2(\omega') \omega' \, d\omega'}{\omega'^2 - \omega^2} \tag{5}
\]

In this section, we investigate the effect of ferromagnetic behaviour based on transition metal (TM) co-doping SnO\(_2\) on optical performance in natural light. The real part \( \varepsilon_1(\omega) \) and the imaginary part \( \varepsilon_2(\omega) \) of SnO\(_2\) pure, (Mn, Mo) co-doped and (Mn, Tc) co-doped SnO\(_2\) are shown in Fig. 6. We have considered the energy range of 0–12 eV. Table 3 lists the computed static dielectric constants using two approximations, GGA-PBE and TB-mBJ, which are raised with the TM added. At lower energies, the real part has a higher value, indicating that the polarization capacity is greater. \( \varepsilon_1(\omega) \) shows negative values in the high energy region, as shown in Fig. 6(a and b), which means that most of the incident light is reflected due to the phenomenon of anomalous dispersion and the materials exhibit metallic
behaviour. We are interested in the imaginary part of the dielectric function in this study to assess the various transitions between the occupied states beneath the Fermi level and the unoccupied states higher than the Fermi level due to photon absorption. From Fig. 6(c and d), the curve of the imaginary part is zero in the low energy region for pure SnO$_2$ due to its high transmission in these regions. This is similar to the calculation performed for SnO$_2$ without doped elements.

Comparing with the (Mn, Mo) co-doped and (Mn, Tc) co-doped SnO$_2$ systems, we can find new peaks in the low energy region. These peaks present interband transitions of the electrons between the top of the valence band and the bottom of the conduction band, which indicate the response of these systems to visible and IR light. The knowledge of the real part and the imaginary part of the dielectric function allows calculation of other optical parameters such as absorption coefficient $\alpha(\omega)$, refractive index $n(\omega)$, loss spectrum $L(\omega)$ and reflectivity $R(\omega)$.

$$\alpha(\omega) = \frac{2\omega(\epsilon(\omega) - \text{Re} \epsilon(\omega))^{1/2}}{c}$$  \((6)\)
where $\mu = \sqrt{\epsilon^2 + \epsilon^2 + \epsilon^2}$.

The absorption coefficient $\alpha(\omega)$ reflects a measure of the intensity of electromagnetic radiation as it crosses through any material. Fig. 7 shows the absorption coefficient spectra as a function of the photon energy of SnO$_2$, (Mn, Mo) and (Mn, Tc) co-doped SnO$_2$. The absorption coefficient curves for both (Mn, Mo) and (Mn, Tc) co-doped SnO$_2$ exhibit new peaks in the lower energies compared to pure SnO$_2$. So, we demonstrate that the introduction of TM brings the visible red-shift phenomenon. The high value of the absorption coefficient in the ultraviolet region contributes to an extremely efficient photon conversion process, which means that a quantum cut may be observed in the systems co-doped with transition metals.$^{17,54,55}$ This result provides a new idea for developing and using SnO$_2$-based optics.

The calculated refractive index $n(\omega)$, reflectivity $R(\omega)$ and loss spectrum $L(\omega)$ using the GGA-PBE and TB-mBJ approach depending on photon energy are displayed in Fig. 8, 9 and 10 for SnO$_2$, Sn$_{1-x}$Mn$_x$Mo$_x$O$_2$ and Sn$_{1-x}$Mn$_x$Tc$_x$O$_2$ with $x = 0.0625$. Table 3 lists the calculated refractive indices at zero energy $n(0)$. We can see that these materials have a high refractive index in the infrared and visible regions, which drops at higher energy in the ultraviolet region. This reduction in value is because of the

$$R(\omega) = \left| \frac{\sqrt{\epsilon(\omega) - 1}}{\sqrt{\epsilon(\omega) + 1}} \right|^2$$

$$L(\omega) = \frac{\epsilon_2(\omega)}{\epsilon_1^2(\omega) + \epsilon_2^2(\omega)}$$

$$n = \sqrt{\frac{1}{2} \left( \epsilon_1^2 + \epsilon_2^2 \right)^{1/2} + \epsilon_1}$$

Fig. 7  Absorption spectra of SnO$_2$ pure, Sn$_{1-x}$Mn$_x$Mo$_x$O$_2$ and Sn$_{1-x}$Mn$_x$Tc$_x$O$_2$ ($x = 0.0625$) by using GGA-PBE (a) and TB-mBJ (b).

Fig. 8  The refractive index of SnO$_2$ pure, Sn$_{1-x}$Mn$_x$Mo$_x$O$_2$ and Sn$_{1-x}$Mn$_x$Tc$_x$O$_2$ ($x = 0.0625$) from (a) GGA-PBE and (b) TB-mBJ.
optical dispersion behaviour of the material. The reflectivity $R(0)$ is given in Table 3, which is less than 18% for all the compounds. The reflectivity increases as we get closer to the high energy zone, as shown in Fig. 9. This reflectivity result can enable these compounds to be used as a selective reflector in the UV region. The loss function describes the energy loss of electrons as they move through a material. The loss occurs when there is a transition between the valence and conduction band. Fig. 10 shows the energy loss function depending on photon energy using GGA-PBE and TB-mBJ approximations. The loss function curve increases gradually with an increase in photon energy. Moreover, the peaks of the electron energy loss $L(\omega)$ spectrum represent the information linked to the plasma resonance and the next frequency to which the electrons respond is recognized as the plasma frequency. Thus, the half-metallic ferromagnet can improve the optical characteristics, such as absorption in visible light transferring electrons from the valence band to the conduction band, which is required for greater photovoltaic conversion.

3.4 Thermoelectric properties

The thermoelectric effect contributes to the conversion of energy, which can be electrical energy generated from heat. A great thermoelectric material has a large value for the electrical conductivity ($\sigma$), which can limit the internal Joule heat loss, a high Seebeck coefficient ($S$) to deliver the greatest possible voltage, and a low thermal conductivity ($K = K_e + K_l$) where $K_e$ is the electronic thermal conductivity due to the charge carriers and $K_l$ represents the contribution due to the thermal vibrations of the network (phonons). To decouple the $\sigma/\tau$ and $K/\tau$, we have considered the constant relaxation time ($\tau = 10^{-14}$ s). These properties are executed in the BoltzTraP code, utilizing the Boltzmann semiclassical theory. After that, the calculation
Fig. 11 (a) Seebeck coefficient, (b) electrical conductivity, (c) thermal conductivity and (d) power factor as a function of chemical potential for Sn$_{1-x}$Mn$_x$Mo$_2$O$_5$.

is done by the GGA-mBJ approximation. The Seebeck coefficient depicts the ability to create an electric potential from a temperature gradient. From Fig. 11a and 12a, we can see that the positive $S$ values are high, indicating the holes are the majority carriers and the dominant role of p-type behaviour for instigating a potential difference. The Seebeck coefficient ($S$) curves for both Sn$_{1-x}$Mn$_x$Mo$_2$O$_5$ and Sn$_{1-x}$Mn$_x$Te$_2$O$_5$ compounds exhibit a decreasing trend with increasing temperature. The high Seebeck coefficient values of these materials at low temperatures, especially at room temperature, make them potential low-temperature thermoelectric materials. The electrical conductivity per relaxation ($\sigma$) as a function of chemical potential ($\mu$) for each temperature is illustrated in Fig. 11b and 12b. We can see that the value of the electrical conductivity of (Mn, Mo/Tc) co-doped SnO$_2$ increases near the Fermi level as the temperature rises, owing to that more electrons can jump from the valence band to the conduction band. As a result, the energized electrons are changed over into charge carriers, which show increasing behaviour with temperature. At room temperature, the values of $\sigma$ are $5.700 \times 10^5$ $\Omega^{-1}$ m$^{-1}$ and $1.700 \times 10^5$ $\Omega^{-1}$ m$^{-1}$ for Sn$_{1-x}$Mn$_x$Mo$_2$O$_5$ and Sn$_{1-x}$Mn$_x$Te$_2$O$_5$ ($x = 0.0625$), respectively. However, the electron part of the thermal conductivity ($K_e$) for both Sn$_{1-x}$Mn$_x$Mo$_2$O$_5$ and Sn$_{1-x}$Mn$_x$Te$_2$O$_5$ are presented in Fig. 11c and 12c. The $K_e$ value increases with the increase in temperature for (Mn, Mo/Tc) co-doped SnO$_2$. In this situation, the high temperatures improve the charge density through electronic vibrations. The crucial factor for selecting the best fit materials for the thermoelectric component is offered by the power factor PF = $S^2\sigma$ [see Fig. 11d and 12d]. The room temperature values of PF for Sn$_{1-x}$Mn$_x$Mo$_2$O$_5$ and Sn$_{1-x}$Mn$_x$Te$_2$O$_5$ are $5.700 \times 10^{-4}$ (V$^2$ K$^{-2}$ $\Omega^{-1}$ m$^{-1}$) and $12 \times 10^{-4}$ (V$^2$ K$^{-2}$ $\Omega^{-1}$ m$^{-1}$), respectively. A material's ability for heat energy conversion into electrical energy is given by the figure of merit, $ZT = S^2\sigma/K_e + K_i$. A $ZT$ value of $\sim$1 indicates the optimum with 30% applicability. The calculation of $ZT$ is tricky and challenging due to the unavailability of a direct approach in calculating $K_i$ and also computationally very expensive. However, we will use the technique to achieve the minimum $K_i$ value by considering the minimum phonon mean free path. The rough estimation of $K_i$ (minimum) is obtained from the bulk modulus and volume relation of the unit cell structure from DFT given by eqn (10):

$$K_i(\text{min}) = 1.2 K_B M_{av}^{1/2} B^{1/2} V^{-1/6}$$

(10)

where $K_B$ is the Boltzmann constant, $M_{av}$ is average atomic mass ($M_{av} = M/nN_A$), $M$ is the molecular mass, $N_A$ is Avogadro’s number, $n$ is number of atoms in the unit cell, $B$ is the bulk modulus, and $V$ is average atomic volume. The minimum $K_i$ values of Sn$_{1-x}$Mn$_x$Mo$_2$O$_5$ and Sn$_{1-x}$Mn$_x$Te$_2$O$_5$ are 11.15 and 3.08 (W m$^{-1}$ K$^{-1}$), respectively. Now considering these $K_i$ as the minimum and $K_e$ values of 3.03 (W m$^{-1}$ K$^{-1}$) and 1.21 (W m$^{-1}$ K$^{-1}$), we could predict the $K_{total} = K_i + K_e$ at 300 K, and consequently a rough estimation of $ZT$ values at RT being 0.114 and
respectively. The results further show that these materials give significant thermoelectric responses at low temperature, although the result is low as compared to the benchmark value of unity at high temperature. Indeed, the presence of all these traits in these ferromagnetic materials, such as the absorption of sunlight, and the ability to convert heat energy into electricity efficiently, indicates that these materials have a high potential for application in thermoelectric devices and could be crucial materials for the development of solar cells as well in the future.

4 Conclusions

In this work, we investigated the electronic, magneto-optical, and thermoelectric properties of \( \text{Sn}_{1-x} \text{Mn}_x \text{Mo}_2 \text{O}_5 \) and \( \text{Sn}_{1-x} \text{Mn}_x \text{TC}_2 \text{O}_5 \) (\( x = 0.0625 \)) based on first principles study using two approximations, GGA-PBE and TB-mBJ. The findings demonstrate that \( \text{SnO}_2 \) doping with double impurities improved the magnetism in the materials so that the half-metallic behaviour was found with 100% polarization at the Fermi level. The mechanisms that control the ferromagnetism in these compounds \( \text{Sn}_{1-x} \text{Mn}_x \text{Mo}_2 \text{O}_5 \) and \( \text{Sn}_{1-x} \text{Mn}_x \text{TC}_2 \text{O}_5 \) are the double Zener exchange and the p–d exchange mechanisms, respectively. The results further show that these materials \( \text{Sn}_{1-x} \text{Mn}_x \text{A}_2 \text{O}_5 \) (\( \text{A} = \text{Mo}/\text{TC} \)) can improve the absorption of sunlight in low energy regions compared to pristine \( \text{SnO}_2 \) and have good thermoelectric properties. Thus, the coupling of these magnetic, optical, and thermoelectric properties in \( \text{Mn}_x \text{A}_2 \text{O}_5 \) co-doped \( \text{SnO}_2 \) systems can predict that these materials are suitable for better efficacy photovoltaic transformation in solar cells.

Conflicts of interest

There are no conflicts to declare.

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