NLTE analysis of Co I/Co II lines in spectra of cool stars with new laboratory hyperfine splitting constants

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ABSTRACT
The analysis of stellar abundances for odd-Z Fe-peak elements requires accurate non-local thermodynamic equilibrium (NLTE) modelling of spectral lines fully taking into account the hyperfine structure (HFS) splitting of lines. Here, we investigate the statistical equilibrium of Co in the atmospheres of cool stars and the influence of NLTE and HFS on the formation of Co lines and abundances. Significant departures from LTE level populations are found for Co I; number densities of excited states in Co II also differ from LTE at low metallicity. The NLTE level populations are used to determine the abundance of Co in solar photosphere, log \( \epsilon = 4.95 \pm 0.04 \) dex, which is in agreement with that in C I meteorites within the combined uncertainties. The spectral lines of Co I were calculated using the results of recent measurements of hyperfine interaction constants by UV Fourier transform spectrometry. For Co II, the first laboratory measurements of HFS A and B factors were performed. These highly accurate A factor measurements (errors of the order of 3–7 per cent) allow, for the first time, reliable modelling of Co II lines in the solar and stellar spectra and, thus, a test of the Co/Fe ionization equilibrium in stellar atmospheres. A differential abundance analysis of Co is carried out for 18 stars in the metallicity range \(-3.12 < [\text{Fe/H}] < 0\). The abundances are derived by the method of spectrum synthesis. At low [Fe/H], NLTE abundance corrections for Co I lines are as large as +0.6, . . . , +0.8 dex. Thus, LTE abundances of Co in metal-poor stars are severely underestimated. The stellar NLTE abundances determined from the single UV line of Co II are lower by \( \sim 0.5–0.6 \) dex. The discrepancy might be attributed to possible blends that have not been accounted for in the solar Co II line and its erroneous oscillator strength. The increasing [Co/Fe] trend in metal-poor stars, as calculated from the Co I lines under NLTE, can be explained if Co is overproduced relative to Fe in massive stars. The models of Galactic chemical evolution are wholly inadequate to describe this trend suggesting that the problem is in supernova yields.

Key words: atomic data – line: formation – line: profiles – stars: abundances.

1 INTRODUCTION
Cobalt is one of the most intriguing elements in studies of galactic chemical evolution (GCE). There is neither an agreement on the overall abundance trend of Co in the halo and thin/thick disc nor a generally accepted scenario for the nucleosynthetic production of cobalt.

Several investigations of Co abundances have been done in various metallicity regimes and stellar populations. All of these abundance investigations were based on Co I lines and local thermodynamic equilibrium (LTE) for the line formation. According to the results of Gratton & Sneden (1991), Co follows the depletion of Fe down to [Fe/H] \( \approx -2.5 \). At lower metallicities, McWilliam et al. (1995) observe a strong increase in cobalt abundance with respect to iron by \( \sim 0.5 \) dex. Del Peloso et al. (2005) obtained a different trend for [Co/Fe], characterized by a steady increase towards supersolar ratios of \( \sim +0.2 \) from [Fe/H] = 0 to \( -0.8 \). An excess of cobalt with respect to iron at \( -4 \leq [\text{Fe/H}] \leq -2.5 \) was reported by Lai et al. (2008), Cayrel et al. (2004) and Ryan, Norris & Bessell (1991). Reddy et al. (2003) and Reddy, Lambert & Allende Prieto (2006) find supersolar and mildly subsolar Co abundances for the thick and thin disc stars, respectively.

The increasing [Co/Fe] ratio with decreasing metallicity was attributed to the Co production in both types of supernovae (SNe) but with uncertain relative contributions (Del Peloso et al. 2005).
However, this is hard to understand from the point of view of stellar nucleosynthesis. Cobalt is an odd-Z element of the Fe group and is produced in α-rich freeze-out in SNe. Thus, its abundance must be sensitive to the explosion entropy and neutron excess available to the progenitor star in the explosive Si-burning phase. The neutron enrichment is determined by the initial metal content of a star and by the previous hydrostatic-burning stages. Hence, in metal-poor environments we expect to see an odd–even effect characterized by a general suppression of the stable odd-Z nuclei relative to their stable even-Z neighbours (Burbidge et al. 1957). Still, this effect is in conflict with the increasing [Co/Fe] trend in metal-poor stars.

Thus far, any attempt to describe the abundances of Co within the framework of explosive nucleosynthesis in SNe failed. Models of GCE, which use standard metallicity-dependent prescriptions for Co production in SNe II (Woosley & Weaver 1995) and SNe Ia (Nomoto, Thielemann & Yokoi 1984; Iwamoto et al. 1999), predict a decreasing or nearly flat [Co/Fe] trend (Timmes, Woosley & Weaver 1995; Samland 1998; Goswami & Prantzos 2000). Models with metallicity-independent SN yields give only a qualitatively similar behaviour; however, large discrepancies with spectroscopic abundances are seen either for the thick disc (Goswami & Prantzos 2000) or for the halo (François et al. 2004).

There are several explanations for the disagreement between observed Co trends and predictions of chemical evolution models. Deficiencies of the latter are hidden among others in the assumed shape of the initial mass function (IMF). As shown by Wang & Silk (1993), the shape of the IMF introduces a factor of 2 in uncertainty to the absolute yield value of an element. The physics of SN explosions is still poorly understood (Thielemann et al. 2007); hence, theoretical stellar yields for Co may be erroneous. It is also important to note that the majority of GCE models assume a single gas phase for the galactic ISM, and only a few consider multiphase ISM (e.g. Schönrich & Binney 2009) that is crucial for a physically accurate description of the galactic chemo-dynamical evolution.

On the other hand, a close examination of the ‘observed’ Co abundances in the Sun and metal-poor stars reveals that all of them rely on several coarse assumptions: LTE in the line formation, static 1D atmospheric models and, often, neglect of hyperfine structure (HFS) splitting of lines. The errors in abundances caused by these approximations are hard to predict, especially because effects of NLTE and temperature inhomogeneities are not independent (Asplund 2005). Iron is the only representative of the Fe group for which calculations of 1D NLTE line formation with 3D convective model atmospheres have been performed (Shchukina et al. 2005). NLTE analyses with 1D model atmospheres exist for a number of elements, specifically for Fe (see Korn, Shi & Gehren 2003, and references therein), Sc (Zhang, Gehren & Zhao 2008) and Mn (Bergemann & Gehren 2008). These and other studies prove that the NLTE abundance corrections can be significant at low gravities and/or metallicities. Due to the overionization, NLTE abundances of Mn in metal-poor stars are larger by +0.1, . . . , +0.6 dex than those computed under LTE.

Knowledge of hyperfine structure in odd-Z iron-group elements is essential in calculations of line formation and abundances. The reason is that HFS is not merely a line-broadening mechanism; it modifies absorption over the entire line profile, especially for strong and saturated lines. Thus, neglect of HFS results in wavelength shifts, incorrectly determined damping parameters and erroneous abundances (this last issue is addressed in Holweger & Oertel 1971; Prochaska & McWilliam 2000; Del Peloso et al. 2005). In a strictly differential analysis of stars with respect to the Sun, which is usually preferred in order to minimize other deficiencies of the stellar atmosphere modelling, neglect of HFS for the reference solar spectral lines may lead to systematically underestimated abundance ratios [x/H] in metal-poor stars. The accuracy of the adopted HFS factors is also important, as we will show in this paper. At present, high-resolution measurements of HFS over a wide spectral range are possible with high-resolution Fourier transform spectrometry (FTS). For example, an analysis of Co I was undertaken using over 1000 line profiles acquired with the FT spectrometer at Imperial College and yielded HFS A splitting factors for 297 energy levels, almost all known Co I energy levels (Pickering 1996).

In this paper, we investigate the excitation-ionization equilibrium of Co in stellar atmospheres and predict what errors in abundance calculations occur when NLTE effects and hyperfine splitting of lines are neglected. Given the particular importance of HFS in this context, we have measured hyperfine splitting of Co II energy levels using the technique of FTS. We analyse the abundance of Co in the Sun and compare it with that of meteorites to ascertain the reason for the discrepancies. Furthermore, we compute the NLTE abundances for a sample of 18 stars, which belong to the thin and thick disc and the halo. The evolution of abundance ratios in the Galaxy and some implications for the Fe-peak element nucleosynthesis are discussed.

2 MEASUREMENTS OF THE HYPERFINE STRUCTURE OF CO II LEVELS

2.1 Simple theory

For atoms with non-zero nuclear spin I, the fine structure levels undergo splitting because of the hyperfine interaction between the nucleus and the electrons. In the absence of perturbations, the energy of the hyperfine structure multiplets is given (Kopfermann 1958) by

\[ W_J = W_{J} + \frac{1}{2} J K + B \left( \frac{3}{4} K (K+1) - J(J+1)(I+1) \right) \frac{2J(2J-1)}{2I(2I-1)}, \]

where \( W_J \) is the energy of the fine structure level number \( J \), \( A \) and \( B \) are the magnetic dipole and the electric quadrupole hyperfine interaction constants, respectively, and \( K \) is defined as

\[ K = F(F+1) - J(J+1) - I(I+1) \]

in which \( F \) is the quantum number associated with the total angular momentum of the atom:

\[ F = I + J, \quad I + J - 1, \quad \ldots, \quad |I - J|. \]

The selection rules which govern the hyperfine transitions are \( \Delta F = 0, \pm 1 \) but not \( F = 0 \Rightarrow F = 0 \).

In addition, there are intensity rules (Kuhn 1962): within a hyperfine multiplet the ratio of the sums of the intensities of all transitions from two states with quantum numbers \( F \) and \( F’ \) is in the ratio of their statistical weights \((2F+1):(2F’+1)\).

This simple theory was used in the fitting of HFS of the Co II transitions in this work. For Co, nuclear spin \( I = 7/2 \). No perturbations were evident.

2.2 Experimental details

The spectra used in this work were obtained as part of an extensive measurement of the Co II spectrum, by FTS with cobalt–neon and cobalt–argon hollow cathode lamps as sources, in the wavelength region 1420–33 000 Å (70 422–3000 cm\(^{-1}\), resulting in a doubling of the number of classified lines, over 200 new energy levels.
2.3 Hyperfine structure analysis

The determination of the A and B factors for the Co II energy levels presented in this paper was carried out using an HFS analysis subroutine in the spectrum analysis program xGReMLIN (Nave, Sansonetti & Griesmann 1997). The input information comprises the I value, the J values of both levels, the known intensity ratios of the transition components (Kuhn 1962), the widths of the components (having Gaussian and Lorenzian contributions), the COG of the pattern and, where possible (see below), an A factor for one of the two levels. A large-scale study of Co II HFS is ongoing at Imperial College, and here we report a detailed investigation of A factors for the 3d⁷(‘P)4s a²P₃,₂,₁ levels and for three of the four 3d⁷(‘F)4p 2D²,₃,₁ levels, with immediate application in this work.

It was not possible to determine the electric quadrupole hyperfine interaction constant B to great accuracy, because the contribution of the last term in equation (1) was so small, but B factors are estimated. The analysis was particularly challenging because no previous measurements existed, but with a comprehensive study we were able to set a starting point for the fits of line profiles in cases where an initial guess at the A factors could be made from a characteristic line profile pattern. For example, when one of the A factors of the levels involved in a transition is an order-of-magnitude greater than the other A factor, the line profile has a characteristic ‘flag’ pattern (examples shown in Pickering 1996). These A factors could then be used to find A factors of other levels using different transitions, building up the number of known A factors.

In general, for each level studied the HFS A factor was determined from the analysis of line profiles for between three and six different transitions; however, in the case of the even levels reported here, between seven and 13 line profiles were fitted.

The resolution of the FT spectrometer is such that the linewidths are limited solely by the Doppler widths and so, depending on the size of the A factors, the overall pattern is usually well resolved into individual components in the IR region, but only partly so in the UV. However, even where a set of line profiles did not appear to be resolved into individual components, the fitting still gave consistent sets of A factors.

The high number of fitted lines, the fact that the A factors were relatively large in magnitude compared to those of higher lying odd levels and a good S/N of studied lines gave reliable A factors for the a ⁵P₃,₂,₁ levels with uncertainties ranging between 3 and 7 per cent. However, fitting of line profiles to find the A factors for the four odd z ⁵D⁰ levels was less reliable because of the smaller value of the A factor, resulting in almost no visible structure in the line profile. A factors for these odd levels should be considered to be estimates.

The values determined for the A and B splitting factors are listed in Table 1, and they are the weighted average values from the line fits with weighting dependent on the S/N of the transitions of the individual line fits (Blackwell-Whitehead et al. 2005). The uncertainties listed in Table 1 are estimated from the range of values of each particular A factor, from the standard deviation. In Table 1 the first four columns give, for each level investigated, the configuration, term designation, J value and energy reported in Pickering et al. (1998). The fifth and sixth columns give the A factor and its uncertainty in mK (1 mK = 0.001 cm⁻¹) determined in this work. The next column lists, where appropriate, approximate values of B factors and their uncertainty. The final column gives the number of line profiles fitted in the process of finding that A factor. An example of a fitted line profile used in this work is shown in Fig. 1.

| Configuration | Term | J | Energy (cm⁻¹) | A (mK) | err (mK) | B (mK) | Err (mK) | N |
|---------------|------|---|---------------|--------|----------|--------|---------|---|
| 3d⁷(‘P)4s   | a ⁵P | 3 |  17771.506  |  40.0 |  3       | −20    |  30     | 10 |
|              |      | 2 |  18031.426  |  49.9 | 1.5      |  20    |  30     | 13 |
|              |      | 1 |  18338.639  |  60.0 |  2       |  2     |  5      |  7 |
| 3d⁷(‘F)4p   | z ⁵D⁰| 4 |  46320.829  |   9.0 |  2       |  10    |  50     |  3 |
|              |      | 3 |  47039.102  |   8.0 |  20      | −      | −       |  1 |
|              |      | 2 |  47537.362  |   8.0 |  20      | −      | −       |  1 |
|              |      | 1 |  47486.778  | <10   | −        | −      | −       | −  |

Note. N denotes the number of profiles fitted. ‘Transitions could not be reliably fitted as part of this work to date; ‘transitions involving ⁵D⁰ were observed to be narrow, consistent with A < 10 mK, but fitting was unreliable, so an upper limit of the A factor alone is given here as a guide.
### 3 NLTE LINE FORMATION

#### 3.1 The methods, model atmospheres and stellar parameters

The statistical equilibrium (SE) calculations for Co are carried out with the DETAIL code (Butler & Giddings 1985), with the radiative transfer based on the method of accelerated lambda iteration.

Spectrum synthesis is performed using the SiU code written by J. Reetz. The profiles of Co i and Co ii lines are computed with NLTE atomic level populations from SE calculations. Radiation damping is derived from the oscillator strengths of transitions. Damping due to quadratic Stark and van der Waals effects follows the expressions given by Unsöld (1955). However, the atomic interaction parameter $C_b$ is calculated using the line half-widths due to elastic collisions with H computed from the theory of Anstee & O’Mara (1995). The log $C_b$ values and other parameters for each Co line investigated in this work are given in Table 2.

The hyperfine structure of lines is taken into account by superposing individually synthesized HFS components. Relative intensities of the components are calculated according to the tables of White & Eliason (1933). Wavelengths are computed using the laboratory data for $A$ and $B$ factors. HFS data for all Co i levels are taken from Pickering (1996). For the levels of Co ii, we use our new values as described in Section 2. The $A$ and $B$ factors are given in Table A1 available online (see Supporting Information).

Abundances are determined by fitting the synthetic lines to the observed line profiles. The analysis of stars is strictly differential relative to the Sun, i.e. any abundance estimate derived from a single line in a spectrum of a metal-poor star is referred to that from the corresponding solar line. This excludes the use of oscillator strengths in calculation of stellar [Co/Fe] ratios.

All computations, including determinations of stellar parameters, are based on the model atmospheres computed with the MAFAGS code. These are static 1D plane-parallel models with line blanketing computed with opacity distribution functions of Kurucz (1992). Convection is taken into account using the mixing-length theory (Böhm-Vitense 1958) with the mixing length parameter $\alpha = 0.5$. Some examples and tests of MAFAGS-ODF models are given in Grupp (2004). Note that due to physical limitations of such classical 1D LTE models, our analysis is restricted to turn-off stars. Only one giant, HD 122563, is included for purposes of comparison with other studies.

The basic parameters for the program stars were adopted from Fuhrmann (2004), Gehren et al. (2004, 2006) and Mashonkina et al. (2008). These analyses make use of the following methods. The effective temperatures were derived by fitting the observed Hα and

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**Table 2.** Lines of Co i and Co ii selected for solar and stellar abundance calculations.

| $\lambda$ (Å) | Mult. | $N$ | $E_{\text{low}}$ (eV) | Lower level | Upper level | $W_\lambda$ (mÅ) | $\log g f^a$ | Log $C_b$ |
|---------------|-------|-----|----------------------|-------------|-------------|-----------------|-------------|----------|
| Co i          |       |     |                      |             |             |                 |             |          |
| 3845.470*    | 34    | 4   | 0.92 $a^2$F$_{7/2}$  | $y^2$G$_{9/2}$ | 120 | 0.01 2 | -31.5 |
| 3957.930*    | 18    | 3   | 0.58 $b$^4$F$_{5/2}$ | $z^4$D$_{3/2}$ | 60 | -2.07 2 | -31.7 |
| 4020.905*    | 16    | 6   | 0.43 $b$^4$F$_{9/2}$ | $z^4$D$_{5/2}$ | 76 | -2.04 1 | -31.8 |
| 4066.360*    | 30    | 3   | 0.92 $a^2$F$_{7/2}$  | $y^2$D$_{5/2}$ | 59 | -1.60 1 | -31.6 |
| 4110.530     | 29    | 6   | 1.05 $a^2$F$_{7/2}$  | $z^2$G$_{9/2}$ | 95 | -1.08 2 | -31.6 |
| 4121.320     | 28    | 4   | 0.92 $a^2$F$_{7/2}$  | $z^2$G$_{9/2}$ | 131 | -0.30 1 | -31.7 |
| 4792.862*    | 158   | 6   | 3.25 $z^6$G$_{11/2}$ | $e^6$F$_{5/2}$ | 34 | -0.07 3 | -30.5 |
| 4813.480*    | 158   | 7   | 3.22 $z^6$G$_{11/2}$ | $e^6$F$_{5/2}$ | 44 | 0.05 3 | -30.5 |
| 4867.870*    | 158   | 10  | 3.17 $z^6$G$_{11/2}$ | $e^6$F$_{5/2}$ | 60 | 0.23 3 | -30.6 |
| 5212.691     | 170   | 9   | 3.51 $z^4$F$_{9/2}$  | $f^4$F$_{7/2}$ | 25 | -0.11 2 | -30.5 |
| 5280.631     | 172   | 8   | 3.63 $z^4$G$_{0/2}$  | $f^4$F$_{9/2}$ | 20 | -0.03 2 | -30.4 |
| 5301.047     | 39    | 5   | 1.71 $a^4$P$_{5/2}$  | $y^4$D$_{5/2}$ | 21 | -1.94 1 | -31.5 |
| 5331.460     | 39    | 5   | 1.78 $a^4$P$_{1/2}$  | $y^4$D$_{5/2}$ | 17 | -1.99 1 | -31.5 |
| 5352.049     | 172   | 9   | 3.58 $z^4$G$_{11/2}$ | $f^4$F$_{9/2}$ | 26 | 0.06 2 | -30.5 |
| 5369.590*    | 39    | 4   | 1.74 $a^4$P$_{3/2}$  | $y^4$D$_{5/2}$ | 44 | -1.59 1 | -31.5 |
| 5483.340     | 39    | 7   | 1.71 $a^4$P$_{3/2}$  | $y^4$D$_{5/2}$ | 51 | -1.41 1 | -31.5 |
| 5647.234     | 112   | 6   | 2.28 $a^4$P$_{3/2}$  | $y^4$D$_{5/2}$ | 14 | -1.56 2 | -31.4 |
| 6189.000*    | 37    | 9   | 1.71 $a^4$P$_{5/2}$  | $z^4$D$_{5/2}$ | 11 | -2.45 2 | -31.7 |
| 6454.990     | 174   | 8   | 3.13 $z^4$D$_{3/2}$  | $e^4$F$_{9/2}$ | 15 | -0.25 2 | -30.4 |
| 6814.950*    | 54    | 5   | 1.96 $b$^4$P$_{3/2}$ | $z^4$D$_{5/2}$ | 19 | -1.90 2 | -31.7 |
| 7417.380*    | 89    | 8   | 2.04 $a^2$D$_{3/2}$  | $z^4$D$_{5/2}$ | 11 | -2.07 2 | -31.7 |
| 7712.661*    | 126   | 8   | 2.04 $b$^2$P$_{3/2}$ | $z^2$D$_{5/2}$ | 10 | -1.57 2 | -31.5 |

Co ii

| 3501.730     | 2     | 8   | 2.19 $a^3$P$_{3}$   | $z^3$D$_{3/2}$ | 86 | -1.22 4 | -32.2 |

Note. $N$ denotes the number of HFS components for a line and the multiplet is specified in the 2D column. $E_{\text{low}}$ is the excitation energy of the lower level of a transition. $W_\lambda$ refers to the line-equivalent width. An asterisk in the wavelength entry refers to the lines, which are not used in determination of the solar Co abundance due to blending or inaccurate log $g f$. $^a$References: (1) Nitz et al. (1999); (2) Cardon et al. (1982); (3) Kurucz & Peytremann (1996) and (4) Raassen et al. (1998).
Hβ profiles under the LTE assumption. The surface gravities were calculated using parallaxes \( \pi \) measured by Hipparcos (ESA 1997) and bolometric corrections were taken from Alonso, Arribas & Martinez-Roger (1995). Masses were determined from the tracks of VandenBerg et al. (2000) by interpolating in the \( M_{bol} - T_{eff} \) diagram. The iron abundances and microturbulent velocities were obtained from FeII line profile fitting in LTE. For the thick disc and halo stars, the abundances of \( \alpha \) elements are enhanced by ~0.4 dex. The population identification is based on stellar kinematic properties, ages and abundance ratios [Al/Mg]. All stellar parameters are listed in Table 3.

### 3.2 Atomic model

The model of the Co atom is constructed as follows. The number of levels and transitions is 246 and 6027 for CoI and 165 and 2539 for CoII. The energy separation of the highest excited level from the continuum is 0.4 eV for CoI and ~3 eV for CoII. Energies of levels and wavelengths of transitions are taken from Pickering & Thorne (1996) and Pickering et al. (1998). The oscillator strengths are adopted from the Kurucz data base (Kurucz & Bell 1995), which includes laboratory measurements and data calculated using scaled Thomas–Fermi–Dirac radial wavefunctions. A complete Grotian diagram for Co is available online (Fig. A1 – see Supporting Information).

Hyperfine splitting of the levels was not included in the SE calculations, since relative populations of HFS components are thermal. Moreover, for the uppermost terms above 6.3 eV in CoI, the fine structure is not maintained. These terms are represented by a single level with a weighted mean of statistical weights and ionization frequencies of their fine structure levels. The transitions between two combined levels are also grouped and the oscillator strength of a resulting line is the average of \( \log g f_i \) weighted according to the appropriate lower level statistical weights.

Since no quantum-mechanical calculations of photoionization for CoI and CoII are available, hydrogenic approximation is used. The cross-sections are computed from the formula of Kramer (Menzel & Pekeris 1935) corrected for the ion charge (see e.g. Rutten 2003) and using the effective hydrogen-like main quantum number. For cross-sections of collisional ionization by e\(^{-}\), we use the formula of Seaton (1962). The rates of allowed and forbidden bound–bound transitions due to collisions with electrons are calculated using the formulae of van Regemorter (1962) and Allen (1973), respectively.

In subsequent sections, we study the influence of photoionization cross-sections and inelastic collisions with hydrogen on populations of atomic levels in Co. However, it should be kept in mind that values for cross-sections have only an order-of-magnitude accuracy.

### 4 RESULTS

#### 4.1 Statistical equilibrium of Co

To discuss the excitation-ionization equilibrium of Co in stellar atmospheres, we use the notation of the departure coefficient \( b_i \), which is defined as \( b_i = N^{\text{NLTE}}_i / N^{\text{LTE}}_i \) with \( N_i \) being the number density of atoms in level \( i \). The \( b_i \) factors as a function of optical depth at 500 nm are presented in Fig. 2 for the solar model atmosphere and several stellar models from the grid. A few selected levels, typical for their depth dependence, are indicated by heavier black traces; the remaining bulk of the CoI and CoII levels is indicated by grey lines.

#### 4.1.1 The Sun

Fig. 2(a) shows the departure coefficients, calculated with our reference model of Co for the Sun. The overall underpopulation of all Co I levels is due to the overionization mainly from the levels of...
are in thermal equilibrium with its ground state. The character of processes leading to NLTE effects in Co does not change for stellar atmospheres with parameters of cool turn-off stars, which form the basis of our abundance analysis. 

4.1.2 Metal-poor stars

The character of processes leading to NLTE effects in Co does not change for stellar atmospheres with parameters of cool turn-off stars, which form the basis of our abundance analysis.

Fig. 2(d) demonstrates the effect of increasing temperature on the departure coefficients of selected Co i and Co ii levels. At \( T_{\text{eff}} = 6400 \text{ K} \), the ionization equilibrium Co i/Co ii is somewhat different from that of the solar model. Nearly 98 per cent of Co atoms are in a singly ionized stage; hence, the ground state of Co ii is not sensitive to overionization from the Co i levels. The level \( a^2F_4 \) keeps its thermodynamic equilibrium value. However, departure coefficients in Co i show larger deviations from unity. The reason is that a stellar flux maximum is shifted to shorter wavelengths; thus, overionization...
The difference in abundances required to fit NLTE and LTE profiles is
and Co = −0.3. This is characteristic of all Co = − levels with
g = 3501.7 = 401, I 1 at line formation depths. As a
6082.5 T ∼−3 and 4), the NLTE
ground state
increases with decreasing [Fe/H] from
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− log = 5500 with the
is no longer coupled
b = eff are positive; for the
log = 5 = 1800 Å. In contrast, in the solar model overionization is important
as a result, NLTE line formation for giants and
dwarfs can be different for transitions involving different levels.
This is evident by comparing the runs of
b = 3.3). This exception is
3 (Fig. 4, top). It is clear
ε 6082.3 ∼A = 49 mK).

4.2 NLTE and HFS effects on the line formation

The computed profiles for selected lines of Co i and Co ii are com-
pared with the solar spectrum in Fig. 3. The synthetic profiles were
calculated under LTE and NLTE conditions, with and without HFS.

All lines selected for the abundance analysis in the Sun and metal-poor stars are relatively weak (Table 2). Hence, the Co i lines
computed under NLTE behave similarly: they are uniformly weak-
ened compared to the LTE profiles. The main effect is the shift of
the optical depth scale due to b1 < 1 at line formation depths. As a
result, the NLTE abundance corrections2 Δ NLTE are positive; for the
majority of Co i lines computed with the solar model atmosphere,
Δ NLTE ∼+0.15 dex.

NLTE abundance corrections for different stellar parameters are
given in Table 4. These values are computed only for five Co i lines and one Co ii line, which can be detected in our spectra of stars
with [Fe/H] < −0.5. Although it is not our goal to investigate giant
stars, we have performed test calculations for the cool giant model
(T eff = 4800 K, log g = 1.8, [Fe/H] = −3.3). This exception is
made because many analyses of Co abundances refer to bright cool
giants with low [Fe/H]. NLTE corrections from Table 4 should only
be used to get a crude estimate of deviations from LTE in metal-
poor stars due to the dependence of the NLTE correction on the Co
abundance.

The main stellar parameter that determines the sign and magnitude
of the NLTE abundance corrections is metallicity. Low metal
abundances lead to decreasing number density of free electrons and
reduced line absorption in the UV, so that the effect of overion-
ization on the opacity of Co i lines monotonously increases. On
average, Δ NLTE increases with decreasing [Fe/H] from ∼0.1 dex for

2 The difference in abundances required to fit NLTE and LTE profiles is
referred to as the NLTE (abundance) correction Δ NLTE = log ε NLTE −
log ε LTE. 

Figure 3. The lines of Co i(4121, 6082 Å) and Co ii(3501 Å) in the solar flux
spectrum (filled circles). Synthetic NLTE and LTE profiles with and without
HFS are labelled correspondingly. Wavelength positions and relative line
strengths of the HFS components are indicated. Note that the relative HFS
component intensities are not on the same scale in figures. The long-dashed
trace on the bottom figure indicates the NLTE profile computed with A =
49 mK for the lower level aP 3 (our reference value is A = 40 mK).

[Fe/H] = 0 to ∼0.7 dex for [Fe/H] = −3 (Fig. 4, top). It is clear
that in addition to the effect of metallicity, high temperatures control
overionization at higher [Fe/H], whereas at low [Fe/H] the effect of
low log g is more important.

The response of NLTE corrections for Co i to the effective tem-
perature is not uniform. At moderate gravities (log g = 4), the NLTE
corrections are maximal in the warm model T = 5500 with the
smallest metallicity (see Table 4). Lower NLTE corrections at even
higher temperatures are due to the increased rates of collisions. At
low temperatures, NLTE abundance corrections are also smaller
Table 4. NLTE abundance corrections for lines of Co i and Co ii calculated with selected models of the grid.

| $T_{\text{eff}}$/log $g$/[Fe/H] | $\Delta_{\text{NLTE}}$ |
|-----------------------------|-----------------|
| wavelength (Å)              | 3501 | 3845 | 3957 | 4020 | 4110 | 4121 |
| 4800/1.8–3.3                | 0.12 | 0.92 | 0.82 |   -- | 0.88 | 0.88 |
| 5000/3/0                    | −0.03| 0.07 | 0.11 | 0.15 | 0.07 |   -- |
| 5000/3/−1                   | −0.03| 0.20 | 0.26 | 0.25 | 0.28 | 0.22 |
| 5000/3/−2                   | 0.02 | 0.64 | 0.60 | 0.64 | 0.48 | 0.76 |
| 5000/3/−3                   | 0.13 | 1.03 | 0.85 |   -- | 0.69 | 0.85 |
| 5000/4/0                    | −0.04| 0.03 | 0.05 | 0.08 | 0.15 | 0.04 |
| 5000/4/−1                   | −0.04| 0.13 | 0.17 | 0.18 | 0.28 | 0.15 |
| 5000/4/−2                   | −0.03| 0.45 | 0.44 | 0.47 | 0.48 | 0.62 |
| 5000/4/−3                   | 0.08 | 0.67 |   -- |   -- | 0.69 | 0.66 |
| 5500/4/0                    | −0.03| 0.08 | 0.12 | 0.12 | 0.23 | 0.1  |
| 5500/4/−1                   | −0.01| 0.27 | 0.3  | 0.32 | 0.36 | 0.35 |
| 5500/4/−2                   | 0.02 | 0.66 |   -- | 0.63 | 0.63 | 0.67 |
| 5500/4/−3                   | 0.17 | 0.75 |   -- |   -- |   -- | 0.14 |
| 5780/4/0                    | −0.02| 0.11 | 0.14 | 0.12 | 0.23 | 0.1  |
| 6000/4/0                    | −0.02| 0.11 | 0.15 | 0.18 | 0.22 | 0.13 |
| 6000/4/−1                   | 0.01 | 0.4  | 0.39 | 0.39 | 0.4  | 0.47 |
| 6000/4/−2                   | 0.06 | 0.64 |   -- |   -- | 0.63 | 0.63 |
| 6000/4/−3                   | 0.31 | 0.69 |   -- |   -- |   -- | 0.7  |
| 6200/3/4/0                  | −0.02| 0.15 | 0.17 | 0.18 | 0.23 | 0.16 |
| 6200/3/4/1.2                | 0.01 | 0.5  | 0.47 | 0.46 | 0.47 | 0.52 |
| 6200/3/4/2.4                | 0.11 | 0.65 |   -- |   -- |   -- | 0.64 |
| 6200/4/6/0                  | −0.01| 0.1  | 0.13 | 0.13 | 0.17 | 0.12 |
| 6200/6/1.2                  | 0.01 | 0.43 | 0.42 | 0.41 | 0.42 | 0.46 |
| 6200/6/2.4                  | 0.11 | 0.61 |   -- |   -- |   -- | 0.59 |
| 6400/4/2/0                  | −0.01| 0.15 | 0.17 | 0.18 | 0.2  | 0.15 |

Note. N-dashes refer to the lines with computed NLTE equivalent widths below 1 mA. Collisions with neutral hydrogen are included with the reference scaling factor $\Sigma_H = 0.05$. Note that $\Delta_{\text{NLTE}}$ for the Co ii line at 3501 Å are also given for the cases when its equivalent width is below 1 mA.

Figure 4. NLTE abundance corrections $\Delta_{\text{NLTE}}$ calculated for the lines of Co i (4121 Å, top) and Co ii (3501 Å, bottom). Calculations are performed for 16 models with $T_{\text{eff}} = 5000, 5500, 6000 \text{ K}$; $\log g = 3, 4$; $[\text{Fe/H}] = 0, −1, −2, −3$.

because the stellar flux maximum is shifted to longer wavelengths, away from ionization thresholds of the important Co i levels.

NLTE corrections increase with decreasing surface gravity. However, for different metallicities and supersolar temperatures, reduction of $\log g$ from 4.6 to 3.4 changes the NLTE abundance corrections for all lines only by $−0.03$–$0.06$ dex. In contrast, $\Delta_{\text{NLTE}}$ strongly depends on stellar gravity in the cool model with $T_{\text{eff}} \leq 5000$. The extreme values of $\Delta_{\text{NLTE}}$ are found for the cool giant model with a subsolar temperature $T_{\text{eff}} = 4800 \text{ K}$, $[\text{Fe/H}] = −3.3$ and a very low gravity $\log g = 1.8$. This is an expected result, because all collisional interactions become very weak due to the small metallicity and gravity, and the role of radiative processes increases in spite of the reduced temperature.

The NLTE corrections for the Co ii line show a different behaviour, which is related to the deviation of the line source function $S'_l$ from the Planck function $B_l(T_s)$. As an example, we study the formation of the Co ii line at 3501 Å. It seems to be relatively unblended in the solar spectrum and can be used to test the ionization equilibrium of Co in the metal-poor stars. In the solar model, this line is sufficiently strong; its core is formed in the upper layers via the photon pumping mechanism, $b_i < b_f$. The line source function becomes superthermal, $S'_{\lambda} > B_{\lambda}(T_s)$, and the line is weakened compared to the LTE case. The same mechanism is responsible for the positive NLTE abundance corrections in the models with $[\text{Fe/H}] \leq −2$. At very low metallicities (Fig. 4, bottom), NLTE corrections are as large as $+0.2, \ldots, +0.3$ dex, depending on the temperature. Consequently, the analysis of Co ii lines in very metal-poor stars can lead to substantial errors in abundances if NLTE effects are neglected.

The errors in abundances introduced by neglecting HFS depend on the line strength. For the solar model, the abundances derived for saturated lines 4121 and 3501 Å without HFS are overestimated by 0.4 and 0.9 dex, respectively. The reason is that HFS effectively desaturates strong lines leading to a compound profile, where the strength of each component is more linearly proportional to the element abundance. Also note that saturated lines are also sensitive to the A and B factors used in calculations of HFS. For example, the 3501 Å HFS line computed with an approximate estimate $A = 49 \text{ mK}$ for the lower level $^2P_3$ (taken from Pickering et al. 1998) cannot fit the observed profile at all (Fig. 3, bottom). In contrast, our new reference value $A = 40 \text{ mK}$ provides an excellent fit to the observed profile. The weak lines, such as 6082 Å, are less affected: the profile computed with all HFS components gives $−0.1$ dex lower abundance. At low metallicity, $[\text{Fe/H}] = −2$, the abundances are almost insensitive to inclusion of HFS in spectrum synthesis; the errors for all investigated lines are not larger than 0.05 dex.

4.3 Solar abundance of Co

The solar spectrum is calculated using the MAFAGS-OIF model atmosphere with $T_{\text{eff}} = 5780 \text{ K}$, $\log g = 4.44$, $[\text{Fe/H}] = 0$ and a constant microturbulence velocity $\xi = 0.9 \text{ km s}^{-1}$ for all lines. The Co line profiles are broadened by a rotation velocity $V_{\text{rot}} = 1.8 \text{ km s}^{-1}$ and by a macroturbulence velocity $V_{\text{mic}} = 2.5, \ldots, 4 \text{ km s}^{-1}$. The observed flux spectrum is taken from the Kitt Peak Solar Flux Atlas (Kurucz et al. 1984).

The lines of Co i and Co ii selected for abundance calculations are listed in Table 2. Measured oscillator strengths are available only for 17 out of 20 lines. Two reference sources of experimental $log g f$ values are Cardon et al. (1982) and Nitz et al. (1999), respectively. For three yellow lines of multiplet 158, we had to adopt the theoretical values of Kurucz & Peytremann (1996). However, the accuracy of calculated data is unknown; hence, the lines of multiplet 158 are only used in the differential abundance analysis of metal-poor stars.
Our final estimate of the solar Co abundance is based solely on the experimental $\log g f$ values. Three lines in the near-UV, 3845, 3957 and 4066 Å, are also neglected in solar calculations due to severe blending.

Fig. 5 shows NLTE and LTE abundances for 16 lines of Co I as a function of their oscillator strengths. A weak trend of individual abundances with $gf$ values, as well as a similar line-to-line scatter under NLTE and LTE, points at the errors in $\log g f$s. For the weak lines, the errors are $\sim$15–25 per cent (Cardon et al. 1982). Two weak lines at 6189 and 6814 Å show NLTE and LTE abundances deviating from the mean by $\geq 0.1$ dex. The lines at 7417 and 7712 Å contain a well-resolved blend in their wings, which is, however, not present in our line list. The line at 5369 Å gives very large abundance, 5.15 dex. As its $gf$ value seems to be reliable, it is likely that the line contains an unidentified blend. We ignore these five lines in the solar analysis, and our sample is further reduced to 11 lines. No significant correlation of individual NLTE or LTE abundances is found with the excitation potential of the lower level or equivalent width of the lines.

The average NLTE and LTE abundances of Co in the solar atmosphere are $\log e_{\text{Co}}^{\text{NLTE},6}\bigg|_{\odot} = 4.95 \pm 0.04$ dex and $\log e_{\text{Co}}^{\text{LTE},6}\bigg|_{\odot} = 4.81 \pm 0.05$ dex, respectively. The standard deviations are quoted as errors. When calculated with the $\log g f$ data from Cardon et al. (1982), $\log e_{\text{Co}}^{\text{NLTE},6}\bigg|_{\odot} = 4.96 \pm 0.06$ dex. This value is nearly equal to the NLTE abundance calculated using five lines with oscillator strengths from Nitz et al. (1999), $\log e_{\text{Co}}^{\text{NLTE},6} = 4.98 \pm 0.03$.

It is interesting that there is a large difference of 0.14 dex between the solar NLTE and LTE abundances determined from the Co I lines with $S_H = 0.05$. Up to now, such a strong NLTE abundance effect has been demonstrated only for Sc I, with $\Delta_{\text{NLTE}} \sim 0.18$ dex derived using $S_H = 0.1$ (Zhang et al. 2008). The average solar NLTE corrections for the other Fe-peak elements, Fe (Gehren, Korn & Shi 2001b) and Mn (Bergemann & Gehren 2007), are smaller. This is, however, not surprising because the magnitude of NLTE effects strongly depends on the model atom used in calculations, in particular on the collision efficiency with hydrogen atoms $S_H$ (see Section 3.2) and the detailed atomic properties, such as separation of energy levels, number and strength of transitions, and ionization potential. Weaker NLTE effects for Mn I ($\Delta_{\text{NLTE}} \sim 0.05$ dex) compared to Co I are due to the differences in the atomic models: (1) the number of low-excitation levels, which stipulate overionization; (2) collisional coupling to the continuum (the latter issue was also emphasized in Gehren et al. 2001b), which amplifies recombination; and (3) the general number of levels. The model of the Fe I atom used by Gehren et al. (2001a) is different from our Co I model in several aspects. The authors adopted $S_H = 5$ as their final value and forced thermalization of the Fe I levels with excitation energy above 7.3 eV. Assuming no explicit thermalization, as we do in the current work, Gehren et al. (2001a) obtain very strong NLTE effects on Fe I lines even for the model with $S_H = 5$, $\Delta_{\text{NLTE}} \sim 0.12$ dex. Using this large scaling factor for H I collisions, we derive the average NLTE abundance correction for Co I lines $\Delta_{\text{NLTE}} \sim 0.06$ dex. Thus, we see no reason to force thermalization of the upper Co I levels. In contrast, we consider collisions with H I as the main source of $\log e_{\text{Co}}^{\text{NLTE}}$ uncertainty. We performed a series of NLTE abundance calculations with $0 \leq S_H \leq 5$. The NLTE result for $S_H = 0$, $\log e_{\text{Co}}^{\text{NLTE}} = 4.96 \pm 0.04$, is almost identical to the case of $S_H = 0.05$. Also, with a scaling factor increasing from 0.5 to 5, the abundance steadily decreases from 4.91 to 4.87 dex with the standard deviation remaining constant, $\sigma \approx 0.04$ dex. Thus, no conclusion can be drawn concerning the optimum value of the scaling factor to hydrogen collisions.

The majority of Co I lines are weak, and they are not sensitive to the van der Waals damping neither are they affected by the microturbulence. We found only one line at 4121 Å, which gives different abundances with the variation of $\xi_t$ or log $C_e$. For $\Delta \xi = \pm 0.2$ km s$^{-1}$, $\Delta \log \epsilon = \pm 0.1$ dex; $\Delta \log C_e = \pm 0.5$ corresponds to $\Delta \log \epsilon = \pm 0.12$ dex. With $\log C_e = -31.63$ calculated using the Anstee & O'Mara (1995) theory and $\xi = 0.9$ km s$^{-1}$, this line gives an NLTE abundance of 4.95 dex, which is consistent with abundances derived from the other Co I lines. Moreover, the standard deviation of the average Co NLTE abundance, $\sigma = 0.04$ dex, is already smaller than the errors given for the oscillator strengths. Hence, we have not tried to adjust damping constants and microturbulence any further.

We checked the ionization equilibrium of Co for the Sun, using the relatively unblended line of ionized cobalt Co II at 3501 Å (Fig. 3, bottom). The line is saturated and consists of eight HFS components, which were calculated with our new hyperfine splitting constants. To produce a better fit to the observed profile, the A factor for the upper level was decreased by 1 mK; this is within the errors of the measured HFS value. Using the theoretical oscillator strength from Raassen et al. (1998), $\log g f = -1.22$, we derive $\log e_{\text{Co}}^{\text{NLTE}} = 4.86$ and $\log e_{\text{Co}}^{\text{LTE}} = 4.88$ dex. With the experimental $gf$ value from Salih, Lawler & Whaling (1985), $\log g f = -1.18$, the NLTE and LTE abundances are $\log e_{\text{Co}}^{\text{NLTE}} = 4.82$ and $\log e_{\text{Co}}^{\text{LTE}} = 4.84$ dex, respectively. We do not assign any error to these values for the reasons described in the following paragraph.

The $\sim 0.1$ dex discrepancy between the lines of Co I and Co II in NLTE is most likely due to the erroneous abundance from the Co II line. First, the uncertainty due to the continuum placement and blending in the near-UV window of the solar spectrum is large. At present, there is no information about other strong lines overlapping with the 3501 Å line of Co II. However, if atomic physics experiments or theoretical calculations reveal the presence of a strong blend, the Co abundance determined from the UV Co I line will be reduced. The accuracy of the calculated oscillator strength provided by Raassen et al. (1998) is not known, whereas the accuracy of the Salih et al. (1985) $gf$-value for the 3501 Å line is not better than 50 per cent, which translates to abundance uncertainty of $\sim 0.2$ dex. If the problem is concealed in hydrogen collisions, a very large scaling factor $S_H \geq 5$ is needed to bring two ionization stages in agreement. This issue will be further investigated in the next section devoted to the metal-poor stars.
The abundance of Co in C1 meteorites is $4.87 \pm 0.01$ dex (Asplund et al. 2009). It is only slightly lower than our NLTE abundance $\log e_{\text{Co}, \odot}^{\text{NLTE}} = 4.95 \pm 0.04$ dex derived from Co I lines. The LTE abundance from the Co II line (4.88 dex) agrees to the meteoritic value if the theoretical $gf$ value from Raassen et al. (1998) is used. Previously, the photospheric LTE abundance from the Co I lines was determined by Cardon et al. (1982), $\log e_{\text{Co}, \odot} = 4.92 \pm 0.08$ dex. This value is $\sim 0.1$ dex higher than our LTE abundance, which is due to several reasons. First, the authors used the semi-empirical model atmosphere of Holweger (1967), which is essentially the same as the model of Holweger & Müller (1974). The latter model is known to give higher abundances compared to the theoretical model atmospheres. Second, equivalent widths were used to measure the abundances. This method always gives only an upper limit on the abundance, because the contribution to a line strength from blending lines is neglected. In all other respects (oscillator strengths, microturbulence, line set), our study and the analysis of Cardon et al. (1982) are similar.

4.4 Abundances in metal-poor stars

Our sample of 17 objects from Bergemann (2008) was expanded by one subdwarf G 64-12 with [Fe/H] = $-3.12$. The UVES spectrum for G 64-12 was taken from ESO/ST-ECF Science Archive Facility (PID 67.D-0554(A)). Other stars were observed with the UVES echelle spectrograph (ESO VLT UT2, Chile) in 2001 and/or with the FOCES echelle spectrograph (CAHA observatory, Calar Alto) during 1999 and 2000. The data for HD 61421 and HD 84937 were taken from the UVESPOP survey (Bagnulo et al. 2003). The UVES data cover a spectral range from 3300 to 7000 Å, whereas FOCES spectra are cut at 4000 Å. A detailed description of the observational material can be found in Bergemann (2008) and Bergemann & Gehren (2008).

The abundance ratios for Co with respect to Fe in stars of our sample are given in Table 3. The Co abundances of thick disc stars with $-1 < [\text{Fe/H}] < -0$ are based on six to 10 lines, which have $W_{\lambda} > 20$ mÅ in the solar spectrum. In the spectra of the halo stars, only a few lines of Co I ($\lambda\lambda3845, 4020, 4110, 4121$) are detected. Due to a systematic abundance offset of $\sim 0.2$ dex between the line at 4110 Å and the other Co I lines, this near-UV line was excluded from stellar analysis. The discrepancy might be related to the poor modelling of H8 inner wings, where the 4110 Å line is located, or to a blend. In fact, no Co abundance studies in metal-poor stars include the line at 4110 Å. For G 64-12, the abundance is based on the single Co I line at 3845 Å, and the error bar $\pm 0.1$ dex reflects the uncertainty of the line fitting due to the low S/N (S/N $\sim 120$) in the near-UV spectral window. We could not determine the solar $\log (g f e)_{\odot}$ value for the 3845 Å line; hence, all stellar abundances based on the line were calculated using the experimental $\log g f$ value of 0.01 from Cardon et al. (1982).

Our sample of 17 objects from Bergemann (2008) was expanded by one subdwarf G 64-12 with [Fe/H] = $-3.12$. The UVES spectrum for G 64-12 was taken from ESO/ST-ECF Science Archive Facility (PID 67.D-0554(A)). Other stars were observed with the UVES echelle spectrograph (ESO VLT UT2, Chile) in 2001 and/or with the FOCES echelle spectrograph (CAHA observatory, Calar Alto) during 1999 and 2000. The data for HD 61421 and HD 84937 were taken from the UVESPOP survey (Bagnulo et al. 2003). The UVES data cover a spectral range from 3300 to 7000 Å, whereas FOCES spectra are cut at 4000 Å. A detailed description of the observational material can be found in Bergemann (2008) and Bergemann & Gehren (2008).

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The [Co/Fe]–[Fe/H] relation, along with the results of other authors, is demonstrated in Fig. 6. Note that the solar NLTE and LTE [Co/Fe] values are set to 0 by definition. The NLTE abundances of Co in the metal-poor stars are higher than the LTE abundances by 0.4–0.7 dex. Thus, instead of the flat [Co/Fe] trend in metal-poor stars, we find that the [Co/Fe] ratio increases with decreasing metallicity down to [Fe/H] $\sim -2$ and is roughly constant thereafter. Two stars with very low NLTE and LTE [Co/Fe] ratios are HD 25329 and HD 103095, respectively. These stars were also analysed by Peterson (1981), who derived [Co/Fe] = $+0.48$ and [Co/Fe] = $+0.15$ for HD 25329 and HD 103095, respectively. The discrepancy with our values stems from different model parameters and abundance analysis techniques. In particular, Peterson used log $gf$ values calibrated on solar lines to calculate the abundances from line-equivalent widths, and the Unsöld approximation for log $C_6$ values was assumed.

Our LTE abundances are generally consistent with LTE results of the other authors considered here, although in the metal-poor domain Co abundances show a large scatter within a study and between studies (Fig. 6). The general trend is hard to define, although the majority of studies indicate that Co is increasing with respect to iron towards very low metallicities. For the thick disc stars our [Co/Fe] trend with [Fe/H] is flat and slightly supersolar, in agreement with Reddy et al. (2006). The thin disc star, Procyon, supports mild underabundance of Co in the thin disc as follows from the results of Reddy et al. (2003). The average Co abundances for stars [Fe/H] $< -1$ are consistent with Johnson (2002) as to slope, absolute values and dispersion. Note that Johnson analysed only giants.

In the attempt to check the ionization equilibrium of Co, we calculated differential abundances from the 3501 Å line of Co II. This line can be discerned from the continuum only in the spectra of five stars. Thus, these abundances must be treated, at best, as upper limits because of a poor S/N below 4000 Å. The NLTE abundance corrections for Co II are not so small and positive. For HD 84937 and HD 140283, $\Delta[\text{Co/Fe}]_{\text{NLTE}} - \Delta[\text{Co/Fe}]_{\text{LTE}}$ $= 0.14$ and $+0.11$ dex, respectively, whereas for HD 102200, HD 34328 and HD 122563, the NLTE corrections are $+0.04$, $+0.04$, and $+0.07$ dex. A significant discrepancy still remains between abundances determined from the lines of Co I and Co II.

Consistent ionization equilibria under NLTE require either significantly lower abundances from the neutral lines and/or much higher abundances from the ionic line. The former can be achieved by increasing the scaling factor to the H I emission cross-sections, $S_H$. Test calculations were performed for two stars. The NLTE results for HD 34328 computed with $S_H = 1$ are not very different from the case of $S_H = 0.05$ (our reference value): the abundance from the Co I lines decreased by 0.15 dex. It is only with $S_H = 10$ that the discrepancy is solved: $[\text{Co/Fe}]_{\text{NLTE}} = 0.26$, which is in agreement with $[\text{Co/Fe}]_{\text{NLTE}} = 0.21$. The abundances derived from Co I lines are not sensitive to a variation of $S_H$. However, for HD 84937,

$^3$ Co abundance ratios determined from the Co I and Co II lines are denoted as $[\text{Co/Fe}]_I$ and $[\text{Co/Fe}]_II$, respectively.
assumption of $S_{\text{H}} = 10$ leads to $[\text{Co/Fe}] = 0.27$, which is still $\approx 0.2$ dex higher than the NLTE abundance determined from Co I lines. Whether such a large scaling factor is justified is questionable.

Another option is that our model atmospheres are not satisfactory, and granular inhomogeneities will have a large effect on abundances in addition to NLTE. Let us consider Fe, for which calculations of 1.5D NLTE line formation with 3D convective model atmospheres have been performed for the Sun and the metal-poor subgiant HD 140283. Using the Fe I lines, Shchukina, Trujillo Bueno & Asplund (2005) found equal 3D and 1D NLTE abundances for both stars that were interpreted as due to stronger NLTE effects in 3D than in 1D models, which largely cancel large 3D LTE corrections. However, large positive NLTE abundance corrections of $\sim +0.4$ dex were demonstrated at low metallicity for weak Fe II lines in 3D. Recalling that Co I and Fe I have a very similar complex atomic structure with ionization energies differing by $\sim 0.04$ eV, one may expect that 3D will have the same (minor) effect on NLTE-based abundances of Co determined from Co I lines whereas large positive 3D corrections may be necessary for Co II lines. In this case, our metallicities based on LTE abundances from Fe II lines may not necessarily be wrong, because the magnitude of the NLTE effect depends strongly on the choice of the scaling factor $S_{\text{H}}$ to the hydrogen collision cross-sections. This parameter must be separately calibrated for each element on the solar and stellar spectra, and for Fe it may take the values different from those used for Co.

We have also investigated the effect of a temperature enhancement on the abundance analysis by repeating the calculations for HD 102200 with $\Delta T_{\text{eff}} = \pm 100$ K with respect to our reference value $T_{\text{eff}} = 6120$ K. For both ions, the effect turned out to be negligible. With $T_{\text{eff}} = 6220$ K, abundances for Co I lines increased, respectively, by 0.02 and 0.06 dex, and the abundances from the Co II line decreased by $\sim 0.02$ dex. Abundance corrections of the same magnitude but with the reverse sign were derived for lower $T_{\text{eff}}$. Thus, we cannot attribute the ionization equilibrium problem to systematic errors in $T_{\text{eff}}$.

5 COMPARISON WITH CHEMICAL EVOLUTION MODELS

There are several models in the literature that describe the evolution of Co in the Galaxy. The difference between theoretical trends is strikingly large: both the shape of the $[\text{Co/Fe}]$ trend and the magnitude of Co depletion or overproduction relative to Fe in metal-poor stars vary by an order of magnitude. In fact, neither of the GCE models is able to describe our NLTE $[\text{Co/Fe}]$ trend in metal-poor stars. The Goswami & Prantzos (2000) model with metallicity-independent SNe yields gives only a qualitatively similar behaviour, characterized by an increase of $[\text{Co/Fe}]$ ratios towards low metallicities. However, this model gives a very good fit to the LTE Co abundances from the current work and other sources. Closer to our NLTE results is the model of François et al. (2004) with unadjusted metallicity-independent SN yields, but the offset between theoretical calculations and the spectroscopic abundances is still too large, $\sim 0.25$ dex. The chemical evolution models with metallicity-dependent SN yields (Timmes et al. 1995; Samland 1998; Goswami & Prantzos 2000) predict radically different $[\text{Co/Fe}]$ trends, which are ruled out by both NLTE and LTE spectroscopic abundances of Co. The same is true for the results of Arnett (1971) Co evolution calculations, whether with or without hydrostatic carbon burning. This discrepancy was also noted by Arnett, Truran & Woosley (1971) and Arnett (1971), who proposed that the $[\text{Co/Fe}]$ ratio should be strongly correlated with the SN Ia progenitor metal content and the amount of mixing in the ISM. However, the effect that this would have on the abundances in metal-poor stars is unclear.

The conclusion from the NLTE trend of Co in metal-poor stars is that massive stars overproduce Co relative to Fe. The observed decline of $[\text{Co/Fe}]$ at $[\text{Fe/H}] \sim -1$ can be explained by an underproduction of Co in SN Ia, but the possibility that SN II and SN Ia Co yields are metallicity-dependent is also not excluded. However, we see that all chemical evolution models, which utilize metallicity-dependent yields, are inadequate to describe the $[\text{Co/Fe}]$ trend suggesting that the problem is in the stellar yields. This is not unexpected, given the sensitivity of SN yields to the details of explosion. Woosley & Weaver (1995) emphasized that their SN II iron yields could be in error by a factor of 2, ascribing even larger uncertainties to the elements produced in $\alpha$-rich freeze-out due to the great sensitivity of those to the mass cut placement. For deeper mass cuts, more Co is produced. Nakamura et al. (1999) found that an increasing neutron excess increases the Co production. Umeda & Nomoto (2003, 2005) showed that if a large-scale uniform mixing occurs in the inner layers of very massive stars, $M > 25 M_\odot$, then Co is produced more efficiently and the effect is even enhanced for larger explosion energies. In connection with this, Nagataki et al. (1997) demonstrated that the axisymmetric explosion in SN II models also boosts an $\alpha$-rich freeze-out and hence an increased production of Co. Interestingly, the results of massive star nucleosynthesis calculations performed by Heger & Woosley (2008) suggest that there is no need for hypernova to explain element abundance patterns in extremely metal-poor stars. The variety of mechanisms, which could affect the Fe-peak production, is overwhelming (Thielemann et al. 2007). Thus, it is not hard to believe that the disagreement between observations and predictions of chemical evolution models is, at least in part, due to the deficiencies of the latter.

6 CONCLUSIONS

Deviations from LTE for Co I are controlled by overionization in the whole range of stellar parameters considered in this work. Thus, ionization equilibrium of Co is shifted towards lower number densities of Co I atoms compared to LTE. Excitation equilibrium of Co II is also disturbed due to optical line pumping.

NLTE effects on the line formation occur for lines of both ionization stages. For Co I, reduced line opacity stipulated by the overionization leads to general weakening of lines. Lines of Co II are affected by the deviation of line source functions from the Planck function. In the solar model atmosphere, these deviations are small, and it is safe to adopt LTE for Co II. In the models with very low metallicities and supersolar temperatures, NLTE corrections for Co II lines are as large as $+0.3$ dex. NLTE abundance corrections for the lines of Co I vary from $+0.1$ to $+0.6$ dex depending on the metallicity and the effective temperature. Our results for the giant models with low $T_{\text{eff}}$, low log $g$ and low $[\text{Fe/H}]$ suggest that in atmospheres of giants deviations from LTE are larger than in dwarfs, although the main stellar parameter that controls the magnitude of NLTE effects in Co is metallicity.

The solar abundance of Co derived from the NLTE analysis of Co I lines is $4.95 \pm 0.04$ dex, which is 0.13 dex higher than the LTE abundance. The abundance calculated from the single relatively unblended Co II line in the solar spectrum is $4.86$ dex. The discrepancy of 0.09 dex between lines of two ionization stages points either to a failure of the NLTE approach to describe the ionization equilibrium of Co or to an erroneous theoretical oscillator strength for the Co II transition. The NLTE abundances calculated with different scaling factors to cross-sections for H I collisions, $0.05 \leq S_{\text{H}} \leq 5$,
slightly disagree with the Co abundance measured in C₂ meteorites, 4.87 ± 0.01 dex.

For the solar-metallicity stars, the incorrect treatment of hyperfine structure leads to large errors in abundances. For the lines with saturated cores, the neglect of HFS leads to an abundance overestimate by > 0.5 dex. Even the weak lines in the solar spectrum are not free from HFS effects, showing differences of 0.05, . . . , 0.15 dex. The influence of HFS on the line profiles and abundances is negligible in the metal-poor stars, not exceeding 0.05 dex.

The differential abundance analysis of 17 stars with −2.5 ≤ [Fe/H] ≤ 0 demonstrated that the evolution of Co abundances in the Galaxy is radically different from all previously reported trends. The NLTE abundance ratios [Co/Fe] are supersolar for the thick disc stars, and at low metallicities [Co/Fe] are as large as 0.8 dex. This result suggests that Co is overproduced relative to Fe in short-lived massive stars. The GCE models, which utilize metallicity-dependent yields for SNe, predict a qualitatively different [Co/Fe] trend for the metal-poor stars, characterized by a plateau or [Co/Fe] depletion. We relate the discrepancy to the deficiency in SN yields.

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SUPPORTING INFORMATION

Additional Supporting Information may be found in the online version of this article:

Figure A1. Grotrian diagram of the Co I/Co II model atom.

Table A1. HFS constants $A$ and $B$ representing magnetic dipole and electric quadrupole interactions for Co I and Co II levels, respectively.

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