From many body wee parton dynamics to perfect fluid: a standard model for heavy ion collisions

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We discuss a standard model of heavy ion collisions that has emerged both from the experimental results of the RHIC program and associated theoretical developments. We comment briefly on the impact of early results of the LHC program on this picture. We consider how this standard model of heavy ion collisions could be solidified or falsified in future experiments at RHIC, the LHC and a future Electron-Ion Collider.

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1. Introduction

Quantum Chromodynamics (QCD) is the "nearly perfect" theory of the strong interactions [1]. The QCD Lagrangean, expressed in terms of fundamental quark and gluon fields, is rich in symmetries and is parameter free if quarks are taken to be massless. Phenomena in the world where the strong interaction holds sway arise as a consequence of the dynamics of the quark and gluon fields. In particular, the QCD vacuum plays an important role in the structure of strongly interacting matter. A subtle example of the role of the vacuum is chiral symmetry breaking, whereby the masses of light quarks are leveraged via the Nambu-Goldstone mechanism into the much heavier masses of the spectrum of observed hadrons.

Because QCD is a theory where most phenomena are "emergent" phenomena, it is especially interesting to ask what happens to QCD matter when squeezed to ultra-high densities or heated to ultra-high temperatures. The role of the vacuum is greatly modified and strongly interacting matter may behave very differently under extreme conditions relative to those found at low temperatures and densities.

The structure of QCD has immediate consequences for extremely hot and dense matter which resolve puzzles about the strong interactions present since its early days such as, for example, "limiting temperatures". Because of asymptotic freedom, QCD matter asymptotically must be a deconfined system of weakly interacting quarks and gluons [2]. Likewise, for matter at extremely large baryon densities, the close packing of hadrons gives way to quark matter [3]. Because screening of quarks and gluons plays a significant role in the dynamics of QCD matter at high temperatures and densities, such a deconfined state is called a Quark-Gluon Plasma [4]. Our universe was a QGP $\sim 10^{-5}$ seconds after the Big Bang.

Another key feature of QCD is "infrared slavery" at large separations (or low temperatures and densities)--a phenomenon closely related to confinement. As a consequence, the QGP undergoes a transition from deconfined quark-gluon matter to confined hadronic matter. Similarly, chiral symmetry which is restored at high temperatures is broken at lower temperatures. It is therefore clear that the theory must contain a rich phase diagram for variations in temperature and baryon chemical potential. Significant theoretical developments in lattice gauge theory and an explosion of computing power have made it possible to explore aspects of the phase diagram in great detail. We refer the reader to Owe Philipsen’s talk at this conference for details on the latest developments [5].

Our focus here is on heavy ion collisions at ultrarelativistic energies where the aim is to produce deconfined QCD matter in the laboratory--this matter is the hottest and densest matter produced on earth and lasts for $\sim 3 \cdot 10^{-23}$ seconds. We will argue here that a wide range of results from the RHIC experiments coupled with theoretical developments have given rise to a picture of heavy ion collisions on which there is a sufficiently broad consensus for us to describe it as a "standard model" of heavy ion collisions. Formulating a standard model is useful and perhaps essential for an intellectually coherent narrative of the science, to expose clearly possible weak chinks in such armor and to bring clarity to future paths along which the field could develop.

2. A standard model of heavy ion collisions

Exploring the QCD phase diagram at high temperatures and densities in heavy ion collisions
is challenging because the collisions are intensely dynamical processes where contributions to any measured final state can arise from different regions in the space-time evolution of the collision. One therefore needs to understand the entire chronology of the collision starting from the properties of the high energy nuclear wavefunctions. While historically the focus of heavy ion collisions was primarily on understanding the thermal properties of deconfined QCD matter, there has been a gradual realization that other aspects of the collision open additional interesting windows into the many-body dynamics of QCD in collision.

![Figure 1: A standard model of the space-time evolution of heavy ion collisions.](image)

A standard heavy ion model consists of the chronology shown in fig. 1. Before the collision, the nuclear wavefunctions are described by correlated multi-parton states called Color Glass Condensates (CGC). The CGCs shatter in the collision producing deconfined non-equilibrium QCD matter called the Glasma. This Glasma likely thermalizes to form a strongly correlated Quark-Gluon Plasma (sQGP), which subsequently undergoes a cross-over transition to hadronic matter with much lower energy densities. The sQGP flows like a nearly perfect fluid as measured by a very low value for the dimensionless ratio of the shear viscosity to entropy density in the fluid. When the expansion rate of the system exceeds the scattering rate of the hadronic constituents, the matter free streams to the detectors. It is sometimes opined that the earliest stages of the nuclear collision are less likely to be understood than the latter stages. My view is that precisely the opposite may be true—one has some confidence that weak coupling techniques in QCD can be used to systematically compute features of early time dynamics. As the system evolves, weak coupling is less reliable and systematic computations can perhaps be performed for a limited sub-set of the system’s properties\(^1\). Nevertheless, as we shall discuss later, a number of theoretical techniques, in combination with experimental results, can shed considerable light on many-body dynamics in the sQGP.

In the following, we shall briefly summarize the theoretical ideas and the extant empirical evidence for each of the stages of the standard heavy ion model. It is impossible to do full justice to this topic in the limited space available for this talk and I will therefore have to frequently refer the reader to the available literature.

3. **Before the collision: wee parton correlations in the Color Glass Condensate**

The appropriate asymptotics for multi-particle production in QCD is the Regge-Gribov asymp-

\(^1\)This does not mean we have all the answers for early time dynamics in weak coupling. An example is thermalization which is still poorly understood. However, it is less well understood in strong coupling frameworks.
totics of the theory corresponding to $Q^2 = \text{fixed}$, $x_{Bj} \to 0$ and $s \to \infty$. In the framework of the theory where the parton model arises, this limit corresponds to very high parton phase space densities. In contrast, the more highly developed Bjorken asymptotics of the theory, $Q^2 \to \infty$, $s \to \infty$ with $x_{Bj} = \text{fixed}$, corresponds to low occupation numbers and is more appropriate for the description of rare high momentum transfer processes. A natural consequence of Regge-Gribov asymptotics at small $x$ is parton saturation [6], which, in the light front formulation of QCD, corresponds to maximal occupancy of $\sim 1/\alpha_S$ for gauge field modes below a momentum scale $Q_S$, the saturation scale.

An equivalent description[7] of parton saturation in the hadron rest frame corresponds to a small size (dipole) probe of size $\sim 2/Q_S$ scattering off a hotspot within the hadron with unit probability. The high occupancy of saturated gluon modes (for $Q^2 S \gg \Lambda_{QCD}^2$) suggests that the nuclear wavefunction at high energies (or small $x$) can be simply described by classical fields [8]. Furthermore, because $Q_S$ is large, this high occupancy state is weakly coupled and its very non-perturbative behavior can be computed systematically order-by-order in $\alpha_S$ beyond the leading $1/\alpha_S$ classical contribution. The Wilsonian renormalization group (RG) equations that describe the evolution of this high occupancy state with energy are stochastic in nature, which explains why it is described to be a Color Glass Condensate (CGC) [9]. These RG equations, called JIMWLK equations [10], govern the energy evolution of n-point wee parton correlations in the hadron wavefunction. These carry much more information about QCD dynamics than parton distribution functions and are interesting to study in their own right.

What is the evidence for parton saturation and the CGC? An early remarkable phenomenon was geometrical scaling of the inclusive cross-section with $Q^2 / Q^2_S$ [11]. Phenomenological models that incorporate the physics of parton saturation do a very good job of describing HERA inclusive, diffractive and exclusive final states [12], fixed target e+A inclusive data [13] and RHIC A+A multiplicities [14] with an economical and consistent set of parameters. An early success of the saturation picture at RHIC was the description of the centrality dependence of the multiplicity distribution in A+A collisions [15]. The phenomenological saturation models have been shown to give a good description of the LHC p+p data including the n-particle multiplicity distribution[16, 17]. Fig. 2 (left) shows the saturation scale versus impact parameter for three different values of $x$ in p+p collisions extracted from HERA data in two different saturation models. The figure on the right shows the saturation scale as a function of $x$ and $A$. Both plots show the saturation scale in the fundamental representation. In the adjoint, relevant for hadronic collisions, one multiplies the value of $Q^2_S$ shown by $9/4$.

While the phenomenological models work very well, it is more satisfactory to confront next-to-leading order CGC predictions with the data. There has been quite a bit of progress in this direction. The Balitsky-Kovchegov (BK) [18] equation, the large $N_c$ "mean field" equation in the CGC for the dipole forward scattering amplitude (corresponding to a 2-point Wilson line correlator) has now been computed at the next-to-leading log (NLL) level [19]. An evolution equation including the running coupling corrections in the NLL expressions [20] gives good agreement with the HERA inclusive data [21], e+A inclusive data [49] and the forward single inclusive deuteron+gold data from RHIC [22]. More interestingly, it describes [23] the systematics of the disappearance of the away side hadron in di-pion production in deuteron-gold collisions at forward rapidities observed by the STAR collaboration [24]. While theoretical caveats [25, 26] to the predicted result may be quantitatively important, they are unlikely to alter its qualitative features. A more serious obstacle
to this interpretation is from the possibility [27] that an azimuthal angle independent pedestal effect could mask this result. A clean experiment which will be able to settle the issue conclusively is to measure the same final state at a future electron-ion collider [28].

In A+A collisions, most saturation models made predictions for the LHC that were on the low side by $\sim 20\%$ [29] compared to the recently released ALICE data [30] for Pb+Pb collisions at 2.76 TeV/nucleon. Integrated multiplicities themselves are not terribly sensitive to dynamics. A 20% discrepancy in the multiplicity corresponds to a corresponding discrepancy of 10% in $Q_S$, which can easily be accounted for in revised fits. Indeed, when nuclear geometry effects are included, the NLO-BK model predicted a centrality dependence of the multiplicity [31] that shows excellent agreement with the ALICE data.

While each of these comparisons of CGC/saturation models to data in e+p/A, p+p, d+A and A+A collisions can be (and are) challenged, taken together they provide a remarkably consistent and detailed picture of a significant body of data suggesting that saturation effects have been seen and are essential to understanding multi-particle production at high energy colliders. At the LHC (and in forward observables at RHIC), the saturation scale is large enough that weak coupling techniques are applicable. This therefore suggests the exciting possibility that physics previously thought inaccessible is now amenable to systematic computation.

4. The little bang and the Glasma

It was understood early on in QCD that multi-particle production in hadron-hadron collisions arises from the scattering of their wee parton clouds [32]. In the CGC, these are classical fields with their field strengths localized on the Lorentz contracted widths of the nuclei, so to lowest order in the coupling constant (of order $1/\alpha_s$), the scattering of two CGCs is described by the collision of two classical fields. This is equivalent to solving Yang-Mills equations with initial conditions determined by the classical fields for each nucleus [33]. These classical equations have been solved and the single inclusive [34] and more recently the double inclusive [35] distributions determined. To
this lowest order, the classical equations (and particle distributions) are boost invariant. The gauge
field configurations are color screened on distances of order $1/Q_S$ and right after the collisions
are dominated by longitudinal color-electric and color-magnetic fields that carry Chern-Simons
charge \[36\]. The QCD matter corresponding to early time non-equilibrium dynamics has been
dubbed "the Glasma" \[37\].

The classical configurations in the Glasma are far from the whole story. Quantum fluctuations
profundely enrich this picture\(^2\). Before the collision, quantum fluctuations generate large loga-
rithms $\alpha_S \ln(1/x_{1,2})$ that are of the same order as the leading classical term and therefore have to
be resummed at each order in perturbation theory. At each loop order, there are also large multiple
scattering contributions that need to be summed to all orders in $\alpha_S n$, where $n \sim 1/\alpha_S$ is the
density of parton sources. High energy factorization theorems proven recently for inclusive quantities
show that the leading logs in $x$ and multiple scattering contributions can be factorized\(^3\) from the
final state dynamics into universal density matrices that satisfy the JIMWLK equation \[39\] con-
volved with the inclusive observable computed at leading order. Thus correlators of Wilson lines
extracted from $e+A$ scattering can in principle be used as inputs into computing $A+A$ final states.

The high energy factorization theorems are a powerful tool to compute the early stage space-
time evolution of quantities such as the stress-energy tensor or correlators of the stress-energy
tensor \textit{ab initio} in heavy ion collisions. They allow one to compute for instance long range rapidi-
ty correlations of inclusive observables that are sensitive to the earliest times in the collision. A
consequence of the formalism is the Glasma flux tube picture \[40\] where $n$-particle correlations
are simply proportional to $(S_\perp/(1/Q_S^2))^{1-n}$ for $n \geq 2$, the ratio of the nuclear transverse area $S_\perp$
to the area of a flux tube $1/Q_S^2$. These geometrical correlations give rise \[41\] to the negative bino-
mial distribution which explains multiplicity distributions \[17\] and forward-backward multiplicity
correlations \[42\] in hadronic collisions.

Long range rapidity correlations that are sharply collimated around $\Delta \Phi \approx 0$ were observed at
RHIC \[43\]. These structures, called "ridges" based on their visual appearance, are present both
for triggered and untriggered two particle correlations. These ridges are not present in peripheral
events and are most prominent in the most central events. Long range rapidity correlations are in-
teresting because they are a "chronometer" of strong color field dynamics at early times in hadronic
collisions. This is illustrated in fig. 3 (left).

In the Glasma flux tube picture \[40\], the ridge phenomenon is a consequence of the long range rapidity correlations in flux tubes of transverse size $1/Q_S$ formed early in the collision that are
subsequently boosted in the final state by radial flow \[45\]. The radial flow provides the near side
angular collimation. The combination of flux tube structures in the initial state and radial flow
gives an excellent description of the published RHIC data \[46, 47\]. The ALICE collaboration has
presented preliminary evidence of a ridge in Pb+Pb collisions \[48\]–we would expect the amplitude
to follow the trend seen at RHIC and be larger than the RHIC values. At the LHC, one expects the
ridge correlations to show deviations from boost invariance \[49\] for $\Delta \eta > 4$ units and the amplitude
of the ridge to decrease with increasing transverse momentum for the pairs \[53\].

\(^2\)This is fortuitous because the naive leading order picture is not what is seen in experiments.

\(^3\)The underlying basis for this factorization is the observation that the computation of inclusive quantities in field
theories with strong time dependent sources can be formulated as an initial value problem \[38\].
In a recent paper, the CMS collaboration announced the discovery of a ridge in high multiplicity events in p+p collisions \[54\] shown in fig. 3 (right). This effect was predicted \[50\] based on our formalism \[49\] but was not advertised because it was a small effect. We subsequently showed the Glasma flux tubes predictions are in qualitative \[51\] and quantitative agreement with the experimental data \[52\]. We note that long range forward-backward correlations were predicted for p+p collisions at the LHC in a related framework \[55\].

Another effect that is very sensitive to properties of the Glasma is the Chiral Magnetic Effect (CME) \[56\]. This is clever idea that suggests that sphaleron transitions in deconfined matter subject to an external magnetic field can lead to charge separation in the direction of the magnetic field that locally breaks P and CP though of course it is preserved in the event as a whole. The STAR collaboration published data on same and opposite charge separations which appeared consistent with the CME \[57\]. Several recent papers however suggest alternative analyses of the STAR data \[58\]–the RHIC low energy run may help clarify which interpretation is correct. Nevertheless, the CME has stirred a lot of theoretical interest and has ramifications for fields outside heavy ion collisions \[59\].

How the Glasma thermalizes to a QGP is an outstanding problem that has not been solved even in weak coupling despite much theoretical progress in recent years. An important ingredient is the role of instabilities \[60\]. In the CGC framework, unstable quantum fluctuations play an essential role in close analogy to the situation in inflationary cosmology \[61\]. Rapidly growing quantum fluctuations can be resummed; in a toy scalar theory, the corresponding energy-momentum tensor obeys ideal relativistic hydrodynamics \[62\]. If these considerations can be extended to a gauge theory, one could have "hydrodynamic-like" flow without early thermalization.

5. The perfect fluid

A key result of the RHIC experiments is the large flow measured suggesting that hydrodynamics is applicable. Hydrodynamics is the right effective field theory to describe the long wavelength, late time behavior of quantum field theory. The surprise at RHIC is that it works at much earlier times than simple estimates would suggest. A powerful measure of the degree of flow is \(v_2\), the second moment of the anisotropy in the single particle distribution. Specifically, it measures how effi-
ciently hot matter converts spatial anisotropies in the initial distribution to momentum anisotropies at later times—the most efficient way to do this is by applying ideal relativistic hydrodynamics.

A quantitative measure of the efficiency of flow is given by the ratio $\eta/s$ of the shear viscosity to the entropy density in the fluid. For simplified boost-invariant ("Bjorken") hydrodynamics, the viscous contribution to the evolution in proper time $\tau$ of the energy density relative to the ideal term is given by $\eta/s/\tau T$; because $1/\tau T \sim O(1)$, this contribution is small when $\eta/s << 1$. In kinetic theory, $\eta/s \approx \tau_{\text{relax}}/\tau_{\text{quant}}$, in units of $\hbar/k_B$, where $\tau_{\text{relax}}$ is the momentum relaxation time in a fluid in response to a shear stress and $\tau_{\text{quant}}$ is the thermal Compton wavelength in the fluid. One therefore expects naively a lower bound of unity on $\eta/s$. However, this expectation is not correct because there is no reason kinetic theory is relevant in this domain. In fact, for strongly correlated systems one expects kinetic theory to fail\(^4\). Nevertheless, on very general grounds one expects a lower bound on $\eta/s$. Is there such a bound and how does the value extracted from RHIC experiments compare?

While the answer to the first part of the question is not known definitively, there is a conjectured lower bound\(^5\) of $\eta/s = 1/4\pi$ \([63]\). This bound was derived for N=4 supersymmetric Yang-Mills (SYM) theory and makes use of the Maldacena AdS/CFT conjecture relating SYM field theory in 4 dimensions to 10 dimensional classical gravity in a background of D3 branes \([65]\). Specifically, the viscosity in SYM is related to the absorption cross-section of a graviton on a black brane, which like the entropy density, is proportional to the area of the brane.

What is $\eta/s$ extracted empirically? For this one relies on viscous hydrodynamic models—the algorithms for these have developed significantly \([66]\). While there are uncertainties related to the initial conditions and other details of the numerical implementation, its probably safe to say that $\eta/s \leq 0.4$ \([67]\). A comparison of $\eta/s$ in various fluids at temperatures close to the critical temperature is shown in fig. 4 (left). These values of $\eta/s$ are much lower than that of water or even liquid helium but are comparable to those of strongly correlated lithium-6 atoms in the unitarity limit. It is remarkable that two systems whose temperatures differ by $10^{19}$ and viscosities by $10^{26}$ flow nearly identically.

Most weak coupling estimates of $\eta/s$ in the QGP give values for $\eta/s$ that are significantly larger \([68]\). Does this rule out a weak coupling description of flow completely? One way out is if the system had a small "anomalous" viscosity (as seen in electromagnetic plasmas) which mimics a small kinematic shear viscosity \([71]\). If, as discussed previously, quantum corrections to the Glasma lead to ideal hydrodynamic behavior, this could provide a quantitative mechanism for the "anomalous" early time viscosity. Detailed studies are feasible in near future on how much the empirical lower bound on $\eta/s$ can be moved upwards.

The ALICE collaboration has released first results on $v_2$ seen in Pb+Pb collisions at $\sqrt{s} = 2.76$ TeV/nucleon \([72]\). The integrated $v_2$ is about 30% higher than at RHIC but $v_2(p_\perp)$ is nearly identical to that seen at RHIC. This is what one would expect if a nearly perfect fluid had been formed at RHIC and is consistent with the predictions from viscous hydro models \([73]\)–see fig. 4 (right). If significant entropy were generated, it should impact the centrality dependence of the

\[^4\]Albeit, one should note that kinetic theory often does much better (as is the case for cold atomic gases) than its condition of applicability would suggest.

\[^5\]There are recent suggestions that in certain higher derivative gravity theories an even lower bound may be attained \([64]\).
multiplicity distribution, which is consistent with initial state predictions for both RHIC and the LHC. This centrality dependence also has the potential of constraining the thermalization time of the Glasma [74]. Interesting measurements at RHIC (and in near future at LHC) on \( v_2 \) fluctuations and higher moments of the anisotropy distribution are quite sensitive to fine details of the initial conditions and final state effects [75]. For instance, the ratio \( v_4/v_2^2 \) gives very different results for different ansätze of the viscous corrections to the single particle distributions at freeze-out [76].

6. Hard probes of QCD matter

Hydrodynamics paints broad brush strokes of the dynamics of strongly correlated matter. To obtain further insight, one looks to hard probes of the QCD medium. Understanding the dynamics of the medium from these is very interesting albeit very challenging as well because a colored hard probe is typically sensitive to the entire time history of the system. At RHIC, it was observed that \( R_{AA} \)–the ratio (normalized by the number of binary nucleon-nucleon collisions) of the inclusive hadron spectrum in A+A collisions relative to the same quantity in p+p collisions–was suppressed by a factor of 5 for \( \pi^0 \)'s and is nearly flat out to the highest \( p_{\perp} \)'s measured at RHIC [77]. A control deuteron+gold measurement [78] established that this phenomenon was a final state effect arising from the interaction of partons with the colored medium.

"Jet quenching" was suggested as a probe of the QGP a long time ago [79] and radiative energy loss by partons traversing the medium was identified as a weak coupling mechanism that would explain it [80, 81]. The energy loss of partons can be related to a transport coefficient \( q \) that characterizes the properties of the medium. There are several formalisms based on the original works that have been developed to confront the heavy ion data on jet quenching [82]. These differ quite a bit in detail and give values of \( q \) that differ considerably--for a clear and interesting recent discussion of the sources of some of these differences, see Ref. [83].

The flat behavior of \( R_{AA} \), the large values of \( v_2(p_{\perp}) \) out to large \( p_{\perp} \), and the unexpectedly large energy loss of heavy quarks are difficult to reconcile in a weak coupling framework without fine tuning. An example of a fine tuning argument is one that explains the flat behavior of \( R_{AA} \) at RHIC as arising from a combination of effects, in particular phase space constraints at large \( x_T \).
that modify the weak coupling prediction that the suppression goes away with increasing $p_\perp$. This should be different at the LHC where there is no large $x_T$ constraint. The first $R_{AA}$ data at LHC for charged hadrons indeed appear to favor this interpretation [84]. One would like however to see the spectrum of $\pi^0$’s and a wider range in $p_\perp$ before more definitive statements are made. An important factor that should be kept in mind while interpreting $R_{AA}$ is the very large initial state gluon shadowing at LHC energies [85, 22].

The apparent strong opacity of the QGP has triggered a considerable amount of work [86] to explain light and heavy quark energy loss in the same AdS/CFT framework that gave us the lower bound on $\eta/s$. There are two sorts of treatments here. In one, the jet production mechanism is treated perturbatively and factorized from the non-perturbative interaction of the jet with the medium [87]. The latter is expressed in terms of correlators of Wilson lines which is computed using the AdS/CFT correspondence. In the other, jet quenching is treated completely in the AdS/CFT framework, typically by looking at the energy loss of heavy quarks [88]. QCD is however significantly different from N=4 SYM, especially in the region around $T_c$, where one notices strong conformal symmetry breaking effects. Until one has a good candidate for a QCD dual in the AdS/CFT framework, perhaps its value is primarily to provide guidance into dynamical questions that one cannot easily answer in the QCD plasma in the region where weak coupling is suspect. For other approaches in addressing this question, see for instance ref. [89].

It is important to understand fully the limits of the applicability of the weak coupling framework. For instance, present treatments of the parton interaction with the medium are at tree level. An interesting quantity to compute is the elastic scattering rate for a hard particle in the medium; the transport coefficient $\hat{q}$ is the second moment of this quantity. The first NLO $O(g)$ computation of this quantity has been reported recently [90]; the correction to the leading order result is significant. The estimate is shown in fig. 5 (right). This raises the question whether resummations a la the pressure in finite temperature field theory are required.

As promised, jets have been produced in copious amounts in Pb+Pb collisions at the LHC. The ATLAS and CMS collaborations confirm observation of jet quenching in di-jets [91, 92]. Looking
at trigger jets with $E_{T1} > 100$ GeV and away side jets in the opposite hemisphere with $E_{T2} > 25$ GeV as a function of the variable $A_J = (E_{T1} - E_{T2})/E_{T1} + E_{T2}$, they find a centrality dependent di-jet asymmetry that is strongest for the most central collisions. At the same time, the vast majority of the di-jets are back-to-back—see fig. 5 (left). A simple explanation [93] that makes intuitive sense follows from the observation that firstly, the softest components of the jet shower decohere sooner and secondly, are more easily deflected out of the jet cone by scattering off the hot medium thereby degrading the energy of the jet, while preserving its angular structure. The first estimates of $\hat{q}$ are consistent with a weak coupling scenario. Clearly, a lot more data can be anticipated in the very near future that will add considerable depth to the existing picture of jet quenching.

7. Looking ahead

I have outlined here the bare bones of a standard model of heavy ion collisions. Even within this structure, there is much that we don’t understand, but we have a better idea of what that is. With LHC very quickly showing us what is possible and the high luminosity and detector upgrades at RHIC on track, we can be optimistic the outstanding issues will be solved. Because many-body QCD is a rich and subtle science, a natural extension of on-going research on hot matter is to explore the complementary many body dynamics of "cold" nuclear matter with a high energy, high luminosity electron-ion collider.

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