Design and Implementation of a Biomolecular Concentration Tracker

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**ABSTRACT:** As a field, synthetic biology strives to engineer increasingly complex artificial systems in living cells. Active feedback in closed loop systems offers a dynamic and adaptive way to ensure constant relative activity independent of intrinsic and extrinsic noise. In this work, we use synthetic protein scaffolds as a modular and tunable mechanism for concentration tracking through negative feedback. Input to the circuit initiates scaffold production, leading to colocalization of a two-component system and resulting in the production of an inhibitory antiscaffold protein. Using a combination of modeling and experimental work, we show that the biomolecular concentration tracker circuit achieves dynamic protein concentration tracking in *Escherichia coli* and that steady state outputs can be tuned.

**KEYWORDS:** feedback circuits, negative feedback, synthetic protein scaffolds, two-component systems, live-cell tracking

Implementation of reliable feedback and control in engineered circuits is a continuing challenge in synthetic biology. Though positive and negative feedback systems are an essential feature of natural biological networks, synthetic circuits more commonly rely on library-based screening to find optimal expression levels. Not only are the resulting systems sensitive to relative concentrations between components, but each time the circuit is expanded, the network of regulatory sequences must be reoptimized to account for increased load on cell machinery. More importantly, this type of open loop approach only optimizes for a single set of environmental parameters, and inherently does not accommodate stochastic cell-to-cell variation, changes due to cell growth cycles, or changes in cell loading from other circuit modules.

Closed loop systems provide regulation of individual components that is robust with respect to environmental disturbances. Negative feedback is a common feature of natural pathways and has been shown to decrease transcriptional response time, to provide stability and reduce fluctuations, and to be necessary for oscillatory behavior.

Active feedback in biological systems has been previously considered at various levels. Recent studies have designed and studied an RNA-based rate regulating circuit with two opposing negative feedback loops, a system utilizing an RNA binding protein to repress translation of its own mRNA and analysis of noise in transcriptional negative feedback. There have also been demonstrations of an in silico closed loop system, in which a computer measured fluorescence output and automatically modulated the activity of a photosensitive transcription factor. In that study, the negative feedback occurred in the software control system outside of the cell.

In this work, we present an *in vivo* protein concentration tracker circuit. To our best knowledge, this is the first demonstration of dynamic molecular tracking entirely within the cell environment. This circuit contains a single negative feedback loop implemented with scaffold proteins and operates on the time scale of one cell cycle. We show that negative feedback implemented through sequestration results in “tracking” behavior: the proportional modulation of one protein concentration (the antiscaffold) relative to that of the reference protein (the scaffold) over a range of reference induction levels.

**RESULTS AND DISCUSSION**

**Scaffold-Based Circuit Design and Implementation.** Previously, Whitaker et al. designed a scaffold-dependent two-component system in which the phosphotransfer was mediated by a synthetic scaffold protein consisting of small protein–protein binding domains. They demonstrated that weak natural cross-talk between a noncognate histidine kinase and response regulator pair could be artificially amplified via colocalization onto the scaffold. By fusing the kinase to the Crk SH3 domain and the response regulator to half of a leucine zipper, both...
Figure 1. Overview of circuit design. (A) The circuit takes an input that sets the reference value. The input proportionally modulates activity of a two-component signaling system that then produces an output. The output triggers a negative feedback response. The negative feedback is the mechanism that generates real-time tracking behavior. (B) The specific implementation of the circuit is shown. The circuit regulates the production of the amount of target protein (antiscaffold–YFP) with respect to the amount of reference protein (scaffold–RFP). Expression of the target is dependent on the amount of free scaffold. The target contains domains that sequester free scaffolding creating a negative feedback loop. Scaffold, response regulator, and phosphatase concentrations are induced via Ptet,P BAD, and Psal, respectively.

Building upon this scaffold-dependent two-component system, we designed a negative feedback circuit by introducing an antiscaffold molecule that competitively inhibits scaffold function. The scaffold molecule consists of a leucine zipper domain (LZX) linked to the SH3 ligand via flexible glycine–serine repeats (Figure 1A). The two-component system is composed of the chimeric kinase Taz linked to four SH3 domains and the response regulator CusR linked to a single leucine zipper (LZX) domain (Figure 1A). The presence of the scaffold recruits the HK Taz and RR CusR into close proximity by forming a ternary complex, resulting in the phosphorylation of CusR. The phosphorylated CusR becomes an active transcription factor, binding to its natural promoter (PCusR) and activating expression of the antiscaffold protein (Figure 1B). The antiscaffold consists of the complementary LZx and SH3 ligand domains, which allow it to competitively bind to and consequently sequester the scaffold protein (K_d = 6 nM for the leucine zipper and K_d = 100 nM for the SH3 domain12,13). This prevents further phosphorylation of the response regulator, and halts further production of the antiscaffold. In the absence of any scaffold protein, no activated response regulator activity is observed (Supplementary Figure S2, Supporting Information).

We implemented the circuit in a ΔCusS ΔCusR Escherichia coli knockout strain. In the absence of CusS, the native bifunctional histidine kinase/phosphatase partner for CusR, activated CusR proteins remain phosphorylated. Accordingly, we reintroduced a CusS(G448A) mutant behind an inducible promoter to tune response regulator deactivation. The G448A mutation disrupts the ATP binding site, eliminating kinase autophosphorylation without affecting phosphatase activity.14,15 This created a tunable phosphate sink in our circuit and ensures tight coupling between present scaffold and activated response regulator concentrations. The negative feedback circuit with the antiscaffold is referred to as the closed loop circuit. As a control, we also built an open loop circuit, in which instead of P_CusR−driven expression of the antiscaffold only the antiscaffold reporter is expressed.

We constructed the circuit as a three plasmid system, in which the kinase is constitutively expressed and the scaffold, response regulator, and phosphatase were cloned behind the inducible promoters Ptet,P BAD, and Psal, respectively. Dynamic tracking behavior was visualized by adding medium strength ssrA degradation tags (C-terminal, RPAANDENYAAV) to the scaffold–red fluorescent protein (RFP) and antiscaffold–yellow fluorescent protein (YFP) fusion proteins.16 The fluorescent reporters mCherry RFP and Venus YFP were chosen on account of their similar maturation times (~5 and 15 min, respectively).17,18

Modeling Dynamics and Steady State Circuit Behavior. The circuit was modeled using differential equations with all chemical reactions between species explicitly defined. The model omits transcriptional activity and accounts only for protein level behavior. With the exception of the antiscaffold production term, all other terms are derived from mass action kinetics. A basic model of the circuit was previously published.19 Here, we have expanded the model by adding the phosphatase species and all accompanying reactions. The 25 species arise from combinations of scaffold (Sc), response regulator (RR), histidine kinase (HK), antiscaffold (AS), and phosphatase (Ph) binding complexes. In total, the model consists of 80 reactions, 25 differential equations, and 26 parameters (See Supporting Information for a complete list of chemical reactions). Many parameters (Table 1) were selected from experimental values found in the literature,20–22 and others were estimated within a physiologically reasonable range.

would be recruited in the presence of a scaffold protein consisting of the SH3 ligand and the other half of the leucine zipper. Forcing the kinase and response regulator into close proximity greatly enhances the level of phosphotransfer and thus the level of downstream expression. The kinase–regulator pair of Taz and CusR was chosen because of measured low levels of cross-talk upon long incubations of purified proteins.11
Model reactions can be classified into five categories: production and degradation, phosphorylation, scaffold complex formation, activation, and irreversible sequestration. Phosphorylated species are denoted with a subscript p (e.g., RRp), and complexes are denoted with a colon separating the participating species (e.g., Sc:AS). Though the possibility of modeling the scaffold as an enzyme-like species was considered, we could not assume that either the kinase or the response regulator would always be in excess, a requirement of the substrate in a Michaelis–Menten reaction. Therefore, Michaelis–Menten kinetics were deliberately avoided.

The production rate, β, of the scaffold, histidine kinase, response regulator, and phosphatase are determined by user input of the total steady state value (in nanomolar) multiplied by the degradation/dilution rate, γ. This ensures constant concentration of these species in solution. The degradation rate γ is applied universally for all species and is estimated based on a cell division time of 30 min.

The phosphorylation reactions describe the autophosphorylation of HK and dephosphorylation of RRp. Key reactions that describe this process are

$$\text{HK} \rightarrow \text{HK}_p$$

$$\text{RR}_p + \text{Ph} \rightarrow \text{RR}_p: \text{Ph} \rightarrow \text{RR} + \text{Ph}$$

The phosphatase forms a complex with the RRp prior to dephosphorylation. We model both phosphorylation and dephosphorylation with a two-step reaction model, an approach consistent with previous models. Rate constants for kinase phosphorylation and dephosphorylation of the response regulator were chosen based on cognate and noncognate phosphorylation rates measured for natural two-component systems and occur on the order of seconds. The following equations show phosphorylation in the absence and presence of inducer:

$$\text{HK}_p + \text{RR}_p \rightarrow \text{HK} + \text{RR}_p$$

$$\text{Sc:HK}_p \rightarrow \text{Sc:HK:RR}_p$$

The degradation/dilution rate, γ, of Sctot0 is applied universally for all species and is estimated based on a cell division time of 30 min. Here we have examples of histidine kinase and response regulator binding to scaffold via SH3 and LZX binding, respectively:

$$\text{Sc} + \text{HK}_p \rightarrow \text{Sc:HK}_p$$

$$\text{Sc:HK}_p + \text{RR}_p \rightarrow \text{Sc:HK:RR}_p$$

A phosphorylated response regulator becomes an active transcription factor. We considered all possible complexes with RRp as possible activators (shown as RRactive). Since the response regulator, CusR, dimerizes upon phosphorylation, the total rate of AS production, kAS, is modeled as a second-order Hill function:

$$\phi \rightarrow \text{AS}$$

$$k_{\text{AS}} = \beta_0 + \left( \frac{\text{RRactive}^2}{K_D^2 + \text{RRactive}^2} \right)$$

where RRactive = RRp + Sc:RRp + Sc:HK:RRp + Sc:HKp:RRp + Sc:RRp:AS.

The negative feedback component comes about through the irreversible sequestration of the scaffold once it has bound to the antiscaffold. We made the assumption that the individual SH3 and LZX domains on the antiscaffold bind independently,

### Table 1. Table of Model Parameters

| parameter | value | units | description |
|-----------|-------|-------|-------------|
| HKtot | 100 | nM | histidine kinase |
| RRintot | 0–3000 | nM | response regulator |
| Scintot | 0–5000 | nM | scaffold |
| Phintot | 0–5000 | nM | phosphatase |
| βAS | 10 | nM s⁻¹ | transcription + translation |
| β0 | 0.01 | | |
Experimental data were normalized by the auto
(B) Steady state experimental data of open and closed loop circuits with and without response regulator matches model predictions. Both sets of
lines show lack of output in the absence of response regulator. Open loop circuit shows sca
output over a range of sca
antisca
production of output is solely due to simulated leaky
with either 0 or 100 nM of response regulator. In the cases with
this can be explained as the sca
significantly with increasing sca
output leads to binding of
protein expression to
Western blot quantification was done with an
analogous circuit containing a bicistronic scaffold (3xFLAG)/
RFP and antiscaffold—GFP (3xFLAG) (Figure S3, Supporting
Information). mCherry is expressed from its own RBS instead
of tethering directly to the sca
concentration of singly bound scaffold increases, decrease in
output is indeed observed (Figure S1A, Supporting Information).

Second, the open loop circuit shows the single sca
occupancy effect at lower concentrations of scaf. In the case of no scaf induction, the open loop circuit has about three times more background than the closed loop circuit. This is due to leakiness in scaffold production in the absence of anhydrotetracycline (aTc). In the closed loop circuit, leaky production of scaffold is subdued by the negative feedback, while in the nonregulated open loop, we see significant production of YFP. All data was normalized to the autofluorescence of a control E. coli strain (Figure S2, Supporting Information).

We compared protein expression to fluorescence output to verify the use of fluorescence traces as a proxy for protein concentration. Western blot quantification was done with an analogous circuit containing a bicistronic scaffold (3xFLAG)/RFP and antiscaffold—GFP (3xFLAG) (Figure S3, Supporting Information). mCherry is expressed from its own RBS instead of tethering directly to the scaffold (12 kDa) to provide a substantial size difference from the antiscaffold (44 kDa). Quantification of band intensities show good agreement between antiscaffold expression and measured fluorescence output (Figure S4, Supporting Information). These results served to validate both the model and the use of synthetic scaffolds as a tunable mechanism for negative feedback.

Characterization of Step Response. We characterized circuit response time by testing the closed loop response to

Figure 2. Open loop versus closed loop. (A) Model predictions of scaffold circuit with and without negative feedback. Solid lines show antiscaffold output over a range of scaffold concentrations (0–1000 nM) for open and closed loop circuits with constant response regulator (100 nM). Dotted lines show lack of output in the absence of response regulator. Open loop circuit shows scaffold single occupancy effect at lower levels of scaffold. (B) Steady state experimental data of open and closed loop circuits with and without response regulator matches model predictions. Both sets of experimental data were normalized by the autofluorescence of a control E. coli strain (Figure S2, Supporting Information).
step inputs. Using a programmable microfluidic plate (CellAsic) under a microscope, step induction of the scaffold protein was achieved by following in 0, 37.5, or 75 nM of aTc (Figure 3A) after 30 min of growth in normal media. Cellular production of response regulator and phosphatase was preinduced by incubating cells with arabinose and salicylate. Microscopy analysis methods are described in Figure S5, Supporting Information. Growth curves for all the conditions are in Figure S7, Supporting Information. In all conditions, expression of scaffold−RFP (Figure 3B) began about 30 min after induction and occurred almost simultaneously with that of antiscaffold−YFP (Figure 3C). Although we had selected mCherry and Venus-YFP on account of their similar maturation times, Venus still matures faster than mCherry (5 and 15 min, respectively). We believe that although there is a delay in mCherry maturation, the scaffold is immediately functional, leading to the near overlap of RFP and YFP expression. In order to better visualize the fold change, fluorescence output is normalized by the maximum value of the lowest step input.

Response times \((T_r)\) for fluorescent detection of scaffold (RFP) and antiscaffold (YFP) were quantified. In control theory, response time is the amount of time needed for an output signal to increase from 10% to 90% of its final steady state. As cells reach stationary phase, circuit expression gradually turns off, and no steady state in fluorescence output is maintained. The 0 nM aTc case shows basal expression of the fluorescent proteins. We observed that scaffold induction, regulated by a \(P_{tet}\) promoter, has a 4-fold increase in expression between 37.5 nM (Figure 3C) and 75 nM (Figure 3D) induction, but only a 2-fold increase in response time (from 50 to 100 min). Antiscaffold output, regulated by the scaffold concentration, shows a 2.5-fold increase in maximum expression and a 3-fold increase in response time (from 40 to 120 min).

This step input characterization revealed that scaffold and antiscaffold fluorescence could be observed almost simultaneously about one cell cycle (30 min) after aTc induction of scaffold transcription. Following induction of the circuit, the response time to maximum expression increases in a linear-like fashion with increasing scaffold induction.

**Circuit Closely Follows Three Step Induction.** Following step input characterization, we investigated circuit response to multiple step-up inputs. Figure 4 shows the results of a three step scaffold induction experiment with 1 h steps corresponding to 50 nM increases of aTc inducer. Growth curves are shown in Figure S8, Supporting Information. The single negative feedback loop in the circuit represses overproduction of antiscaffold, but there is no mechanism for feedback in the case of an excess of scaffold or antiscaffold. As such, the model predicts that increases in inducer will lead to immediate increases of scaffold followed closely by the antiscaffold but once induction is turned off, degradation of proteins depends on the endogenous ClpXP degradation machinery (Figure 4A).
Additionally, the upward slope of each curve should overlap until induction ceases.

Step-up induction was performed on cells preincubated in arabinose and salicylate, activating expression of response regulator and phosphatase, respectively. As shown in Figure 4B, experimental results for a three step induction are consistent with model predictions and show overlapping curves during the ascent, with each individual curve dropping off slowly as induction ceases. The chemical induction of the scaffold produces a much smoother output curve compared with the response regulator-modulated scaffold. Due to high levels of leaky expression, the open loop circuit did not respond to multistep inductions (Figure S8, Supporting Information).

Inducer Diffusion Rates Contribute to Cumulative Effect of Sequential Pulses. We observed in our model that variations in inducer diffusion rate would greatly affect the outcome of sequential pulses (Figure 5A). The removal of aTc from the cytoplasm and surrounding media is not instantaneous, and induction does not go to zero. Growth curves are shown in Figure S9, Supporting Information. Given two sequential 30 min pulses spaced 1 h apart, the diffusion constant determined whether two independent, identical outputs occurred or an additive effect would take place. Essentially, if the first pulse of inducer is not given sufficient time to diffuse out of environment, aTc molecules from the first pulse are still present when the second pulse occurs. We modeled inducer diffusion following a pulse with an exponential decay term, $\beta_{sc} = \beta_{ind}(-rt)$. Figure 5A shows two pulse simulation results when the default decay constant ($r = 2.8 \times 10^{-4}$ s$^{-1}$, middle column) is increased or decreased by 10-fold.

When we tested two pulse induction in vivo (Figure 5B), we ran simultaneous experiments with zero, one, and two 30 min pulses of aTc (50 nM). The single pulse fluorescence maximum (Figure 5B, middle column) was normalized to 1 au. It is clear from the two pulse fluorescence output data that the diffusion rate of aTc after a pulse in vivo was actually much slower than expected in silico. In fact, so much of the scaffold from the first pulse remained that there was almost a 2-fold increase in
maximal expression during the second pulse. This was an effect that had not been apparent previously during the multistep inductions, where we showed sequential increases in inducer concentration. These data show that modulation of pulse frequency, but not concentration, can result in the same additive effect as increasing inducer concentration.

We then sought to improve our model by tuning the inducer decay constant (Figure 5C), generating outputs that demonstrated the nearly 2-fold increase observed \textit{in vivo}. Although the optimized decay rate \((r = 2 \times 10^{-4} \text{ s}^{-1})\) better captured gene expression during log phase, we consistently observed a rapid decrease in fluorescence as cells approached stationary phase.\(^28\) This resulted in improved model performance when simulating dynamic circuit behavior.

**Model-Informed Exploration of Parameter Space.**

Circuit limitations were explored \textit{in silico}. Specifically, we investigated the effects of tuning response regulator and phosphatase concentrations on the ability of the antiscaffold output to track the scaffold reference. Response regulator and phosphatase concentrations are easily accessible parameters via inducible promoters in our experimental system. In Figure 6A, a scan of input–output response curves is shown over a range of response regulator and phosphatase concentrations (See Figure S10, Supporting Information, for explicit values). For each curve in the grid, the scaffold concentration in which the single occupancy drop-off occurs was found, and the slope of the curve up to that concentration was found with a linear fit. The maximum scaffold occupancy limit is the concentration of scaffold molecules at which each scaffold molecule only has either a response regulator or histidine kinase. The slope of the curve up to that point represents the antiscaffold to scaffold ratio that can be achieved by the circuit. In the case where the single occupancy limit does not appear, the last concentration is used. Data shown in Figure 6B indicates that increasing response regulator values result in a greater AS/Sc ratio (up to 1.5-fold increase), while increasing phosphatase serves to bring down that ratio. The effect of increasing phosphatase is apparent when the maximum scaffold occupancy limit is examined (Figure 6C). Furthermore, the simulations show that some minimal amount of phosphatase is necessary for a sufficiently high response regulator turnover rate so as to approach a 1:1 ratio. As phosphatase concentration increases, active response regulators are quickly dephosphorylated,
decreasing the efficacy of the scaffolds, lowering the maximum occupancy concentration, and making the drop-off more steep. Based on experimental outputs of our circuit, however, we believe the actual achievable dynamic range of the circuit is limited to the lower left corner of the parameter space. The qualitatively estimated induction range is shown with the black and gray rectangles in Figure 6B,C.

By modulating response regulator and phosphatase concentrations, a range of maximal expression levels for scaffold and antiscaffold can be achieved. Figure 7A,B shows steady state circuit response to varying levels of response regulator induction in both the model and experimental circuit. Increasing RR concentrations increases the gain of the system by increasing the number of available active transcription factors for the AS promoter. In simulation data (Figure 7A), we see that the scaffold occupancy effect is mitigated by higher levels of response regulator. This is consistent with our previous explanation, since more regulator means almost all free scaffold molecules will exist as Sc:RR. Experimental data for tuning response regulator concentration via 10-fold increases of arabinose (Figure 7B) do not extend the scaffold levels far enough to show the occupancy effect, but the increasing output gain is evident.

The presence of phosphatase in the circuit modulates the amount of time that phosphorylated response regulator is active. Hence, tuning phosphatase concentrations changes $RR \leftrightarrow RR_p$ cycling time. Early versions of the circuit did not include the phosphatase species, and we were unable to observe dynamic behavior due to buildup of $RR_p$. Using the model, we explored the effects of adding a phosphatase prior to testing in vivo. Figure 7C,D shows steady state responses across a range of phosphatase concentrations. Simulation results show that increasing phosphatase decreases overall circuit output (Figure 7C) by decreasing the average time $RR_p$ is active.

Figure 6. Model-based exploration of parameter space. (A) Simulations of scaffold to antiscaffold inputs and outputs over a range of phosphatase (100–5100 nM, 500 nM increments) and response regulator (10–1510 nM, 150 nM increments) concentrations. Enlargement shows the scaffold single occupancy limit concentration and curve fitting for each curve. Red dotted lines show curve fits; the slope represents the antiscaffold to scaffold ratio. (B) Heat map showing antiscaffold to scaffold ratio for each curve shown in part A. Increasing response regulator results in greater AS/Sc ratios. Gray box represents estimated experimental phosphatase induction range. Black box estimates experimental response regulator induction range. (C) Heat map of maximum scaffold occupancy limit. Higher concentrations of phosphatase result in decreased maximum scaffold occupancy limit.
Experimental results (Figure 7D) support model predictions and show this suppression of output with increased induction via salicylate.

In Figure 7E,F, these experimental steady state data are analyzed using the same techniques shown in Figure 6. Figure 7E shows antiscaffold to scaffold ratio and scaffold occupancy limit as calculated based on RFP/YFP fluorescence data with 10-fold increases in response regulator induction (10−100 μM salicylate). There was no additional induction of phosphatase (0 nM salicylate). Figure 7F shows the same metrics with 10-fold increases in salicylate. Response regulator concentration is constant (0−100 μM salicylate). (E) Ratios of YFP/RFP from part B as a proxy for As/Sc ratios with increasing response regulator. Scaffold occupancy limit was not observed in response regulator experiments. (F) Ratios of YFP/RFP and scaffold occupancy limit values from part D with increasing phosphatase. All experimental data was normalized by baseline autofluorescence values.

**Scaffold-Based Circuits for Rapid Feedback.** We have designed a novel negative feedback tracker circuit using modular synthetic scaffold proteins and a two-component system with scaffold-dependent phosphorylation. The use of scaffold proteins for negative feedback could potentially be a robust way of linking modules and ensuring constant performance despite intrinsic and extrinsic noise. Scaffold proteins have been shown to be powerful hubs for organization of regulatory feedback in natural networks, usually by colocalization of phosphorylation machinery. Previous studies have rewired the naturally occurring Ste5 scaffold in the yeast MAPK cascade to redirect signals, to modify delays in signaling time, and to introduce ultrasensitivity. The modular scaffold proteins used in this study were previously used to control phosphotransfer to noncognate response regulators, building a synthetic signaling pathway. Here we have taken those same scaffolding modules and built an entirely synthetic feedback circuit. The system allows for tunable control of output gain and cycling time. Most importantly, the proportional antiscaffold tracking of the scaffold is maintained over a range of component concentrations.
After we designed the circuit framework, we constructed and then experimentally validated an ODE-based mathematical model. Through selection of parameters and reaction rates based on the literature, we obtained a model able to reasonably predict circuit behavior. Comparisons between simulation and experimental data confirmed the presence of scaffold-mediated negative feedback, and we used the model to scan the parameter space in a way that would have been time and resource intensive to explore in vivo. We found that steady state circuit gain can be tuned by changing response regulator concentrations and cycling time is controlled by varying phosphatase levels, observations that were supported by experimental data. Following initial step induction system characterization of step input response time, expression of both the reference (Sc-RFP) and output (AS-YFP) protein was shown to be fast and responsive to multistep inputs. Finally, we found that pulse-modulated induction could result in additive circuit response, leading to improvement of the model through more accurate inducer diffusion parameter values.

A scaffold-based biomolecular tracking circuit has potential applications in active regulation of component expression in synthetic circuits. The relatively small size (approximately 60 AA) of the scaffold and antiscaffold proteins facilitates attachment to larger proteins, represented in this work by mCherry-RFP and Venus-YFP. Rather than open loop tuning of regulatory sequences and large-scale screening, scaffold-based negative feedback could be utilized. By attaching the scaffold to a native protein, it may also be possible to tie synthetic circuit inputs to naturally occurring cycles in vivo. It is well-known that many natural cell processes such as developmental segmentation, circadian clocks, and stem cell multipotency involve oscillatory gene expression.

Furthermore, response to signal transduction may be modulated not by amplitude, but by frequency. We have shown that the scaffold-modulated protein tracker follows changes in both amplitude and frequency and exhibits good agreement with a mass-action model. Future iterations of this design may improve tracking fidelity by including reverse feedback loop to compensate for overexpression.

**METHODS**

**Cell Strain and Media.** The circuit was implemented in the E. coli cell strain WW62, a variant of BW27783 (CGSC 12119) with knockouts of EnvZ, OmpR, CusS, CusR, CpxA, and CpxR. All cell culture was done in optically clear MOPS EZ rich medium (Teknova, M2105), with 0.4% glycerol instead of 0.2% glucose. The use of glycerol as a carbon source was resource intensive to explore. Cell were grown in two consecutive overnight cultures of 0.2% glucose. The use of glycerol as a carbon source was found to be fast and responsive to multistep inputs. Finally, we found that pulse-modulated induction could result in additive circuit response, leading to improvement of the model through more accurate inducer diffusion parameter values.

**Plasmids.** Plasmids used in this study were derived from those used in Whitaker et al. The plasmid encoding the SH3-domain–Lzx histidine kinase and CusS-G448A phosphatase are on a low copy plasmid (p15A) with chloramphenicol resistance. Detailed plasmid maps are shown in Figure S11, Supporting Information, and a complete list of plasmids and strains can also be found in the Supporting Information.

**Plate Reader Experiments.** Plate reader data were collected on a Biotek H1MF machine using the kinetic read feature. Cell were grown in two consecutive overnight cultures in MOPS EZ rich media. On the day of the experiment, overnight cultures were diluted 1:40 and grown to OD ≈ 0.1 prior to the start of the experiment. Cells were incubated in the plate reader at 37 °C and shaken at 800 rpm between reads. Measurements were taken every 5 min. Cells were grown in clear bottomed 96-well microplates (PerkinElmer, ViewPlate, 6005182) and sealed with breathable clear membranes (Sigma-Aldrich, Breath-Easy, Z380059). mCherry was read at excitation/emission of 580/610 nm at a gain setting of 140, Venus was read at 500/540 nm at a gain setting of 100, GFP was read at 488/525 nm at a gain setting of 75.

Analysis of the data was done by taking fluorescence readings at late log phase for each independent well. Experimental conditions were done in triplicate and repeats were averaged. Fluorescence per OD was normalized by the fluorescence of a control strain (lacking mCherry/YFP/GFP) such that the cell autofluorescence equals 1 au (Figure S2, Supporting Information). Error bars shown are standard error of the mean.

**Western Blots.** Cultures were grown for 5 h in a deep-well microplate at 37 °C with a range of aTc from 0–120 nM. Arabinose was kept constant at 0.001%. No salicylate was used. After 5 h, OD600, RFP, and GFP were measured in a plate reader. Western blot samples were collected and spun down. Because aTc concentration can affect growth rates, the volume spun down was calculated based on OD to ensure consistent cell mass. Pellets were resuspended in lysis buffer and boiled for 10 min. Samples were run on 4–20% tris-glycine gels (Novex, 150 V for 1 h), and a semidy transfer apparatus was used (Bio-Rad, 15 V for 20 min) to transfer onto a PVDF membrane. Monoclonal anti-FLAG M2-peroxidase (HRP) antibody was diluted 1:88,000 in 5% milk. Blot imaging was done using the Chemi Hi Resolution setting on a BioRad ChemiDoc MP imager. Quantification of band intensity was done using Image Lab 5.0 (BioRad).

**Microscopy.** Step induction data were taken using the CellAsic ONIX microfluidic perfusion system for bacteria (B04A). The microscope is an Olympus IX81-ZDC enclosed in a custom heater box. Images were taken using a 100X oil immersion phase objective. Fluorescence filters are S80/630 nm for mCherry (Chroma 41027) and S10/560 nm for YFP (Chroma 31040 JP2). Microscope media was augmented with oxidative scavengers Trolox (200 mM) and sodium ascorbate (2 mM).

**Nightscope.** Overnight cultures were then diluted 1:500 in media containing arabinose (0.01%) or salicylate (100 μM) or both 4 h prior to loading in the CellAsic plate. This is to ensure steady state concentrations of response regulator and phosphatase prior to aTc induction of the scaffold. Cells were diluted 1:10 again before loading. Microscopy movies were taken inside a temperature controlled environment set at 37 °C, and images were taken at 10 min intervals. Exposure time was 10 ms for brightfield and 500 ms for mCherry and YFP fluorescent channels.

Analysis of microscope movies was done using custom algorithms in ImageJ and MATLAB. For each frame, the phase...
image is converted to a binary mask of the cell colony. The mask is then used to find total mCherry and YFP fluorescence in the frame. After subtraction of background fluorescence, the total fluorescence is normalized by the total cell area (fluorescence intensity per pixel). For step induction experiments, fluorescence is normalized such that the maximum fluorescence of the lowest concentration induction is equal to 1 au. Figure S5, Supporting Information, shows the microscopy analysis workflow. Error bars shown in microscopy time trace data are the standard error of the mean between analysis of different positions \( n = 7-10 \) on the same experimental plate.

**Model Implementation.** The model was implemented using the Simbiology toolbox in MATLAB and the ode15 solver (See Supporting Information files for MATLAB code).

### ASSOCIATED CONTENT

**Supporting Information**

This material is available free of charge via the Internet at http://pubs.acs.org.

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**Notes**

The authors declare no competing financial interest.

### ACKNOWLEDGMENTS

The authors thank J. Kim for insightful discussion and suggestions on the model, and Y.E. Wang for help with Western blots. This research was conducted with government support under and awarded by DoD, Air Force Office of Scientific Research, National Defense Science and Engineering Graduate (NDSEG) Fellowship, 32 CFR 168a. Additional support was granted in part by the Benjamin M. Rosen Graduate (NDSEG) Fellowship, 32 CFR 168a. Additional support was granted in part by the Benjamin M. Rosen Bioengineering Center, the NIH/NRSA Training Grant 5 T32 GM07616, the Gordon and Betty Moore Foundation through Grant GBMF2809 to the Caltech Programable Molecular Technology Initiative, and the Institute for Collaborative Biotechnologies through Grant W911NF-09-0001 from the U.S. Army Research Office. The content of the information does not necessarily reflect the position or the policy of the Government, and no official endorsement should be inferred.

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