Research Article

Study on Dynamic Constitutive Model of Weakly Consolidated Soft Rock in Western China

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1. Introduction

Most of the mining areas in western China are Jurassic coal seams [1–3], overlying with extremely thick cretaceous water-rich rocks (mainly are fine sandstone, medium sandstone, coarse sandstone, conglomerate, and mud-sandstone interbeddings), which has a large porosity, weak cementation, and low strength [4–6]. Freezing sinking technology is often used in shaft construction, but, in the process of blasting excavation, a number of engineering accidents occurred [7, 8], such as freezing wall leakage and water gushing, which is due to the cognitive deficiency of Cretaceous red sandstone’s mechanical properties under impact load. As the key to represent mechanical properties of rock materials, constitutive relation provides basic parameters for engineering design. Therefore, it is particularly important to study the mechanical properties of such rock under the artificial freezing conditions and impact loads.

At present, many achievements have been made in the study of constitutive models of rock materials under impact load. According to the stress-strain curve’s features of soft rock and concrete under dynamic load, Zhao et al. [9, 10] improved the existing Z–W–T damage model and established a new dynamic constitutive equation. Xie et al. [11] introduced the theory of continuous damage and statistical strength into the simplified overstress constitutive model and established a simplified damage constitutive equation. Aiming to the dynamic mechanical properties of rock-like materials such as hard rock, soft rock, frozen soil, raw coal, and concrete. It can be referred to the parameter determination method in this paper to study and determine the parameters, reduce the difficulty of parameter selection, and improve the practicability of the constitutive model and parameters, so as to guide the engineering practice better.
model of rock using the combination model method. By means of Laplace transform, the damage variables based on pore and fracture deterioration are introduced, and then Cai et al. [14] proposed a new model of the Maxwell body, Bingham body, and damage body in parallel and derived the rock dynamic damage constitutive model relationship at medium and low strain rates. Li et al. [15] developed an excess stress model to analyze the dynamic response of rock joints by using the mechanical conceptual models based on the Hooke, the modified Saint-Venant, and the Newton elements. Wu et al. [16] conducted the sensitivity analysis of the microscopic parameters in the DCA model; meanwhile, he indicated that the model is valid and applicable to describe the dynamic tensile response and can well predict the dynamic tensile strength of rock-like materials. In engineering practice, rocks are in a complex stress state and occurrence environment in most cases. Therefore, it is of great significance to study the constitutive relations of rock materials under the multifactor coupling actions. Therein, on the basis of Z–W–T model, Ma et al. [17, 18] and Zhang et al. [19] introduced the statistical damage theory or used the longitudinal wave velocity to define the damage variable and established the damage dynamic constitutive relation of frozen soil considering the temperature effect. Furthermore, Xie et al. [20] built a micromechanical constitutive model to describe the dynamic compressive deformation of frozen soil and proved the model well reflects the experimental results of frozen soil at different high strain rates and temperatures. Zhang et al. [21] analyzed the dynamic mechanical properties of frozen soil based on HJC constitutive model and used LS-DYNA to simulate the results. According to the dynamic mechanical properties of marble treated at different high temperatures, Wang [22] established a damage evolution equation considering the temperature effect and strain rate effect, which combined the damage theory and strain equivalence principle. It can be seen that the statistical damage theory and strength theory have been widely used in the study of dynamic constitutive relations of rock materials. It lays a foundation and provides the guiding value for the study of mechanical constitutive relation of Cretaceous red sandstone in western China under the freezing temperature field and impact load [23–27]. And the latest research findings in dynamic constitutive model are all about frozen soil. However, few relevant research results have been obtained on the rock’s dynamic constitutive relations under the coupling of stress field, temperature field, damage field, and other multiple fields in the freezing sinking of soft rock.

Due to the complexity and indeterminacy of the constitutive parameters, the constitutive model was often difficult to use in engineering practice. In this research, according to the mechanical properties of weakly consolidated soft rock at different freezing temperatures obtained by the SHPB tests, a dynamic constitutive relation improved by the Z–W–T model was established considering the strain rate effect, temperature effect, and damage effect. In addition, the parameters of the model were analyzed and studied, and the parameter values with high practicability were determined. It could provide the reference and design basis on the mineral resources exploitation of artificial freezing project and infrastructure construction in cold regions.

2. Impact Test of Frozen Red Sandstone

2.1. SHPB Testing System and Testing Contents. A split Hopkinson pressure bar device was used to complete the dynamic uniaxial compressive tests of frozen red sandstone. The main part of the pressure bar is alloy steel with a diameter of 50 mm, density of 7.8 g/cm³, elastic modulus of 210 GPa, and longitudinal wave velocity of 5172 m/s. The impact bullet has a length of 300 mm and a rod diameter of 50 mm. The composition diagram of SHPB test system is shown in Figure 1.

The SHPB impact test is established on the basis of one-dimensional stress wave theory and stress uniformity assumption. In order to realize constant strain rate loading and eliminate wave dispersion effect, a pulse shaping technique is used, which is a copper posted on the contact surface of the incident bar and bullet, and Vaseline was applied on both sides of specimen to reduce the friction effect and end effect. The red sandstone specimen is made into a diameter of 50 mm and a height of 25 mm following the International Society of Rock Mechanics (ISRM) standards. After saturation, it was put into a low-temperature test chamber for more than 48 h. After the completion of impact pressure and system commissioning, it was rapidly transferred and sandwiched between the incident bar and transmitted bar to complete the impact test. The impact test was controlled within 30 s to reduce the heat exchange between the specimen and environment.

According to the temperature field distribution of frozen wall, the temperature of the specimens was set as 0°C, −10°C, −20°C, and −30°C. The impact pressure of SHPB testing system was set as 0.044 MPa, 0.052 MPa, 0.06 MPa, and 0.075 MPa, and the corresponding loading rates were 1800 GPa·s⁻¹, 2000 GPa·s⁻¹, 2200 GPa·s⁻¹, and 2400 GPa·s⁻¹.

2.2. Stress-Strain Curve Analysis. The stress-strain curves of red sandstone under impact load at different freezing temperatures (i.e., 0°C, −10°C, −20°C, and −30°C) are shown in Figure 2. It shows an obvious segmental character and can be divided into four stages: nonlinear compaction stage, linear elastic stage, plastic development stage, and rapid failure stage. This type of sandstone shows obvious initial nonlinear compaction characteristics in statics [19–21]. However, the proportion of the nonlinear compression segment is very small in the dynamics, which is basically not shown in the stress-strain curves. It is because the microcracks and microholes inside the rock cannot completely close under the high-speed impact, and the dynamic strain increases with the stress faster than in statics, so the form of expression is different. The linear elastic stage accounts for a small proportion of the whole stress-strain curve, and the stress in this stage improves rapidly with the increase of the strain. Its tangential slope is the dynamic elastic modulus of red sandstone, and there is a big difference between the elastic modulus of red sandstone under the impact load and
Figure 1: SHPB testing system.

Figure 2: Dynamic stress-strain curves of red sandstone. (a) $T=0^\circ C$. (b) $T=-10^\circ C$. (c) $T=-20^\circ C$. (d) $T=-30^\circ C$. 
static load, which is about 5 to 35 times, showing obvious impact toughness. The plastic development stage accounts for more than 50% of the total stress curve, and the slope at this stage is small, showing an obvious plastic flow characteristics. Due to the weak cementation among the soft rock particles, it can be interpreted as a comprehensive reflection of strain rate hardening effect, strain rate strengthening effect, and thermal softening effect caused by adiabatic temperature rise. It can be seen from the rapid failure stage of the curve that the ability of red sandstone to resist deformation weakened rapidly after the macroscopic crack is generated; then the macroscopic damage is caused by the crack propagation and penetration, and the specimens lost the load capacity without unloading to 0. The decline rate of the rock's postpeak curve is accelerated with the decrease of temperature, which shows the enhancement of brittleness.

As shown in Figure 2, the strain rate of red sandstone under the same loading rate decreases but the peak stress increases with the decrease of temperature, and the corresponding peak strain also changes with temperature. It shows that the temperature effect exists in the mechanical characteristics of such rocks under the impact load, which should be considered into the constitutive model.

3. Constitutive Model of Frozen Red Sandstone

3.1. Z–W–T Constitutive Model. Z–W–T nonlinear viscoelastic constitutive model can well describe the mechanical properties of solid materials in the range of viscoelastic deformation. Therefore, it has been widely used to study the mechanical properties of concrete, perspex, rock, and other materials in the range of strain rate between 10^{-4} s^{-1} and 10^{3} s^{-1}. The model consists of one nonlinear spring body and two Maxwell bodies, as shown in Figure 3. Its constitutive equation is as follows:

$$\sigma = E_0 \varepsilon + a \varepsilon^2 + b \varepsilon^3 + E_1 \int_0^t \dot{\varepsilon} \exp \left( \frac{t - \tau}{\eta_1} \right) d\tau + E_2 \int_0^t \dot{\varepsilon} \exp \left( \frac{t - \tau}{\eta_2} \right) d\tau$$

(1)

The nonlinear spring in the model is used to describe the equilibrium state of stress. Two different Maxwell bodies, respectively, describe the viscoelastic response under different strain rates and only function in their own "effective responsibility region." Therein, the response time of the low-frequency part is 10^{-1} s to 10^{2} s, and the high-frequency part is 10^{-3} s to 10^{-6} s.

3.2. Constitutive Model of Frozen Red Sandstone. When the dynamic constitutive relation of frozen sandstone is expressed by Z–W–T constitutive model, the change of dynamic mechanical relationship under the coupling action of temperature field, damage field, and impact stress field is not considered. And the following improvements are made as follows:

(1) The low-frequency Maxwell body has no time to response in the impact test, so it was simplified to a simple spring with an elastic modulus of $E_1$.

(2) The Cretaceous red sandstone contains a large number of defects such as microcracks and micro-pores. The rock failure process can be regarded as a process of damage development under the impact load. Therefore, the damage body is added in the constitutive model, and the following assumptions are made:

(1) The interior of the rock is continuous and the damage is homogenized.

(2) The impact process is considered to be completed under the constant loading rate.

(3) The microelement strength follows Weibull distribution, and its probability density is

$$\phi(\varepsilon) = \frac{m}{n} \varepsilon^{m-1} \exp \left( \frac{-\varepsilon^m}{n} \right),$$

(2)

where $m$ and $n$ are distribution parameters, which are related to the property and shape of the material.

(3) The interaction between ice crystals and rock particle matrix is enhanced with the decrease of temperature, and the viscosity coefficient is constantly increased. It is the essence of the temperature effect of the mechanical properties of red sandstone under impact load. According to the properties of mechanical elements, the viscous body with viscosity coefficient varying with temperature is added here.

The modified constitutive model is shown in Figure 4. It can be seen that the new model is composed of three parts in parallel, and its stress relation is

$$\sigma = \sigma_1 + \sigma_2 + \sigma_3,$$

(3)

where the stress of the nonlinear body is

$$\sigma_1 = (E_0 + E_1) \varepsilon + a \varepsilon^2 + b \varepsilon^3 = E_3 \varepsilon + a \varepsilon^2 + b \varepsilon^3.$$  

(4)

The Maxwell body is composed of the elastic element and damping element in series, and its relationship between stress and strain is as follows:
The damaged body can be written as follows:

$$\sigma_2(t) = \sigma_{21}(t) = \sigma_{22}(t),$$

$$\varepsilon_2(t) = \varepsilon_{21}(t) + \varepsilon_{22}(t),$$

$$\sigma_{21} = E_2\varepsilon_{21}(t),$$

$$\sigma_{22} = \eta_2\dot{\varepsilon}_{22}(t).$$

4. Experimental Verification of Constitutive Equation

The constitutive equation and determined parameters are used to fit the test curves of red sandstone at different temperatures under impact load, as shown in Figure 5.

According to the creep test of red sandstone at different freezing temperatures, the relation between its viscosity coefficient and temperature is obtained, as shown in

$$\frac{dD}{de} = \phi(e).$$

After integrating (16) and combining with (3), we get

$$D = 1 - \exp\left(-\frac{\varepsilon^n}{n}\right).$$

According to (17), the constitutive relation of the damaged body can be written as follows:

$$\sigma_{31}(t) = (1 - D)E_D\varepsilon(t) = E_D\varepsilon(t)\exp\left(-\frac{\varepsilon^n}{n}\right).$$

The damaged body is in series with viscous body in new model, according to the derivation of (5) to (15), and replacing $E_2$ by $E_D\exp(-\varepsilon^n/n)$, the following can be obtained:

$$\sigma_3(t) = \eta_3\dot{\varepsilon}\left\{1 - \exp\left[-\frac{E_D\varepsilon}{\eta_3\dot{\varepsilon}}\exp\left(-\frac{\varepsilon^n}{n}\right)\right]\right\}.$$

Therefore, the constitutive equation of the modified model is

$$\sigma = E_\Delta\varepsilon + \alpha\varepsilon^2 + \beta\varepsilon^3 + \eta_3\dot{\varepsilon}\left[1 - \exp\left(-\frac{E_D\varepsilon}{\eta_3\dot{\varepsilon}}\exp\left(-\frac{\varepsilon^n}{n}\right)\right)\right] + \eta_3\dot{\varepsilon}\left[1 - \exp\left(-\frac{E_D\varepsilon}{\eta_3\dot{\varepsilon}}\exp\left(-\frac{\varepsilon^n}{n}\right)\right)\right].$$

4.1. Parameter Determination. There are 9 unknown parameters in the constitutive equation. According to the parameter determining method of Z–W–T constitutive model, the quasi-dynamic stress-strain curves of red sandstone at 0°C were fitted to determine the parameters $E_\Delta$, $\alpha$, $\beta$, and $E_2$, as shown in Table 1.

According to the creep test of red sandstone at different freezing temperatures, the relation between its viscosity coefficient and temperature is obtained, as shown in
Figure 6(a). It can be seen that, with the fall of temperature, the viscosity coefficient of red sandstone increases rapidly, which shows an obvious temperature effect. And its fitting relation is
\[ \eta_3 = -13e^{-T/24.3} + 16. \] (21)

The remaining 4 parameters in the constitutive equation were obtained by fitting the stress-strain curves obtained by the impact test.

4.2. Parameter Analysis. Table 2 shows the corresponding fitting parameter’s value of the constitutive equation. It can be seen that the elastic modulus of the damage body \( E_D \) is 9 MPa, which is a fixed value and does not change with the temperature and strain rate. The parameter \( m \) does not change with the strain rate and only relate to the temperature, and its value decreases with the fall of temperature, as shown in Figure 6(b). The relationship is
\[ m = 0.02112e^{T/25.9} + 0.174. \] (22)

The parameter \( n \) decreases with the increase of the strain rate and the amplitude of change is small, which is \( 10^{-3} \). The mean values \( \bar{n} \) of \( n \) at each temperature are 0.0558, 0.0571, 0.0585, and 0.0592. It can be seen that \( \bar{n} \) is increasing with the fall of temperature, as shown in Figure 6(c). The relation between \( \bar{n} \) and the freezing temperature is
\[ \bar{n} = -1.16 \times 10^{-4}T + 0.05591. \] (23)

Figure 6(d) is the data distribution scatter plot of \( \eta_2 \). It can be seen that the value of \( \eta_2 \) increases with the increase of
the loading rate at the same temperature, and the magnitude of change is $10^{-2}$. However, $\eta_2$ does not show a specific similarity law with the decrease of temperature. Generally speaking, it shows rate dependence, and the values of different temperatures can be selected by interpolation method.

In summary, among the 9 unknown parameters in the constitutive equation, there are 5 fixed values that did not change with the temperature and strain rate, and only 2 parameters change with the temperature. Only the parameter $\eta_2$ and $n$ change with temperature and strain rate, and their data range is relatively fixed and the amplitude of change is small. It can be seen that the constitutive equation has few unknown parameters, and its value is relatively fixed. The relevant mechanical parameters can be quantitatively

Table 2: The fitting parameter values of constitutive model.

| $T$ (°C) | Strain rate (s$^{-1}$) | $E_D$ (MPa) | $\eta_2$ | m | n | Strain rate (s$^{-1}$) | $E_D$ (MPa) | $\eta_2$ | m | n |
|----------|------------------------|-------------|----------|----|---|------------------------|-------------|----------|----|---|
| 0        | 112                    | 9           | 0.0433   | 0.195 | 0.0561 | 160                     | 9           | 0.0671   | 0.195 | 0.0557 |
| -10      | 102                    | 9           | 0.0398   | 0.189 | 0.0572 | 144                     | 9           | 0.0690   | 0.189 | 0.05705 |
| -20      | 98                     | 9           | 0.0564   | 0.183 | 0.0589 | 129                     | 9           | 0.0631   | 0.183 | 0.0584 |
| -30      | 88                     | 9           | 0.0880   | 0.181 | 0.05943 | 121                    | 9           | 0.1028   | 0.181 | 0.0592 |
|          | 105                    | 9           | 0.0976   | 0.181 | 0.05934 | 162                    | 9           | 0.1045   | 0.181 | 0.0590 |
calculated according to (21) to (23) in practical engineering applications. Therefore, it has certain practical value.

4.3. Parameter Sensitivity Analysis. A group of experimental data and the corresponding fitting parameter values are randomly selected to analyze the influence of the changing parameters ($\eta_2$, $m$, and $n$) on constitutive equation. Firstly, $\eta_2$ of high-frequency Maxwell body is analyzed, and the influence of its value change to the constitutive curve is observed after fixing the values of other parameter. As shown in Figure 7(a), with the increase of $\eta_2$, the fitting curve-up translation as a whole, and the linear elastic stage becomes longer but the slope remains unchanged. And the shape of the fitting curve does not change. It can be seen that the change of $\eta_2$ only affects the magnitude of the peak strength. Therefore, it is the intensity control parameter.

Figures 7(b) and 7(c) show the influence of Weibull distribution parameters $m$ and $n$ to the curve, respectively. It can be seen that, with the increase of $m$ and $n$, the end of the fitting curve changes from divergence to convergence and the peak stress and corresponding peak strain decrease continuously. Meanwhile, the slope of plastic stage also decreases gradually, and the unloading strength of postpeak curve decreases continuously, which shows an enhancement of the rock’s brittleness. The parameters $m$ and $n$ have the same effect on the curve and jointly control the curve’s plasticity and the failure stage of the development trend. However, from the view of the influence of parameter values on the curve, when the stress curve has the same change, the change of $m$ is 0.0005, but $n$ is 0.0001, so $n$ has a higher sensitivity to the curve.

4.4. Error Analysis. Figure 8 shows the relationship between the difference of red sandstone’s test curve to the constitutive fitting curve and strain at different temperatures. It can be seen that the fitting error ($\Delta \sigma$) fluctuates with the increase of
strain, but the fluctuation is small, which is controlled among −4 Mpa to 4 Mpa. Therefore, the new constitutive model can well reflect the mechanical properties of sandstone under impact load.

In combination with the sensitivity analysis of parameters, several conditions of fitting curve error are explained here. (1) In condition 1, it can be seen that the absolute value of Δσ is large in the initial stage of strain, which is caused by the fact that the small part of nonlinear compression segment appearing in the test curve is not expressed in the fitting curve. (2) In condition 2, the slope of the fitting curve in the plastic development stage is decreasing all the time, while the red sandstone shows the strain hardening stage before reaching the peak strength under the action of the high strain rate, which makes the fitting accuracy declined and Δσ is relatively large. (3) In condition 3, since the variation of elastic modulus with temperature is not considered in the determination of constitutive parameters, there will be fluctuation in the initial section of the error curve. When the value of Δσ is positive, it means that the elastic modulus of the fitting curve is smaller than the actual value, and when Δσ is negative, it means that the elastic modulus of the fitting curve is bigger than the actual value. Therefore, the selection of parameters can be further improved according to the error curves.

5. Applicability Analysis of Constitutive Equation

The constitutive model established in this research has good applicability to describe the dynamic mechanical properties of Cretaceous red sandstone under artificial freezing conditions, and it can be conveniently applied to engineering practice. And the applicability of the constitutive model on other rock materials is further discussed. Since the viscous body in the constitutive equation is considered as the influence of temperature effect on the constitutive relation of red sandstone, it can be treated as an unknown parameter.
Figure 9: Continued.
when characterizing the dynamic properties of other materials. On this basis, the dynamic stress curves of mudstone and sandy mudstone obtained by Zhao et al. [9, 10], the dynamic stress curves of concrete and granite obtained by Zhai et al. [12], the dynamic stress curves of red sandstone obtained by Yan et al. [28], the dynamic stress curves of raw coal obtained by Zhang et al. [29], the dynamic stress curves of frozen soil obtained by Zhang et al. [19], and the dynamic stress curves of limestone obtained by Zou et al. [30] are quoted in this research. The applicability of the constitutive equation is verified, and the fitting results of all materials are shown in Figure 9. It can be seen that the stress curves of each material under impact load are different in shape and have their own features. The strain rate of test data is distributed between $50 \text{s}^{-1}$ and $1000 \text{s}^{-1}$, and the peak strength of the material is distributed between 5 MPa and 500 MPa, with a wide distribution range. From the fitting results of the constitutive equation, the fitting curves and experimental data have good consistency in soft rock, hard rock, frozen soil, concrete, and raw coal, which indicates that the constitutive equation established in this research has good universality in representing the constitutive relations of rock materials.

Table 3 shows the fitting parameters of the constitutive equation for each material. The following was observed. (1) Although there are 9 unknown parameters in the constitutive equation, the values of 5 to 7 constitutive parameters of the same material under different strain rates are the same and do not change with the strain rates. In addition, the fitting parameter values of $\eta_3$ in different materials are the
same, all of which are 1. Therefore, it can be set as a fixed value in practical application. (2) The physical meaning of each parameter value is correct. Among them, the elasticity coefficient in the high-frequency Maxwell body \((E_2)\) is always an order of magnitude larger than the nonlinear body \((E_3)\), which conforms to the rock’s mechanical response mechanism under impact load. (3) Although the nonlinear coefficient \((\alpha \text{ and } \beta)\) are relatively complex in numerical value, they provide the possibility for the constitutive equation to be applied to the universality of rock-like materials.

In conclusion, the applicability of the constitutive equation in the expression of other material’s dynamic properties was further discussed in this paper, but the possible regularity in the fitting parameters of each material was not further studied. In practical engineering applications, the parameters should be studied and determined according to each material’s dynamic properties and the parameter determination method in this research. We cut down the variables as much as possible, so as to reduce the difficulty of parameter selection and improve the practicality of constitutive model and parameters.

6. Conclusions

In this research, a new constitutive model considering the temperature effect, strain rate effect, and damage effect was established based on Z–W–T model. The parameter sensitivity and fitting error were analyzed. And the applicability of constitutive model is further discussed. The conclusions are as follows:

1. According to the stress-strain curve features of red sandstone under impact load, taking the change of rock’s viscosity coefficient with temperature into consideration, a nonlinear viscoelastic damage constitutive model considering the temperature effect, strain rate effect, and damage effect was established by improving the Z–W–T model. Therein, the strength of damage microelement was assumed to follow the Weibull distribution, and its constitutive equation is deduced.

2. The test data are in good agreement with the fitting curves of constitutive equation. The fitting error fluctuates between \(-4\) MPa and \(4\) MPa, the fitting accuracy is 0.95 to 0.99, which shows that the constitutive equation can well represent the dynamic properties of frozen red sandstone, and the model is suitable for studying the dynamic constitutive relation of Cretaceous red sandstone.

3. The fitting parameters of constitutive equation are simple. Sensitivity analysis was carried out for the variable parameters, and \(n_2\) only affects the peak strength, which is the strength control parameter. \(m\) and \(n\) affect the development trend of the plastic stage and failure stage of the curve, but \(n\) has a higher sensitivity to the curve. The physical meaning of each parameter is clear. Meanwhile, the parameter range and the related change rule are determined, which improves the practicability of constitutive model and provides reference and basis for engineering practice.

4. The constitutive model can well reflect the nonlinear characteristics of red sandstone under impact load. It is proved that the constitutive equation is applicable to the dynamic performance characterization of rock materials such as hard rock, soft rock, frozen soil, raw coal, and concrete. In engineering practice, the parameter values can be studied and determined by referring to the parameter determination method in this research, which can reduce the difficulty of parameter selection and improve the practicability of constitutive model.

Data Availability

The data used to support the findings of this study are included within the article.

Conflicts of Interest

The authors declare that there are no conflicts of interest regarding the publication of this paper.

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