Isocost Lines Describe the Cellular Economy of Genetic Circuits

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ABSTRACT Genetic circuits in living cells share transcriptional and translational resources that are available in limited amounts. This leads to unexpected couplings among seemingly unconnected modules, which result in poorly predictable circuit behavior. In this study, we determine these interdependencies between products of different genes by characterizing the economy of how transcriptional and translational resources are allocated to the production of proteins in genetic circuits. We discover that, when expressed from the same plasmid, the combinations of attainable protein concentrations are constrained by a linear relationship, which can be interpreted as an isocost line, a concept used in microeconomics. We created a library of circuits with two reporter genes, one constitutive and the other inducible in the same plasmid, without a regulatory path between them. In agreement with the model predictions, experiments reveal that the isocost line rotates when changing the ribosome binding site strength of the inducible gene and shifts when modifying the plasmid copy number. These results demonstrate that isocost lines can be employed to predict how genetic circuits become coupled when sharing resources and provide design guidelines for minimizing the effects of such couplings.

INTRODUCTION

The ability to predict the behavior of a system from that of the composing modules is a core problem in systems and synthetic biology (1,2). However, prediction accuracy is still limited as modules display context-dependent behavior, wherein the function of circuits is affected by direct or indirect interactions with surrounding cellular components and resources (3). One cause of context-dependence is the fact that different circuits share common cellular resources that are available in limited amounts. When new genes are introduced into a cell, resources involved in their expression have to be redirected. In the model organism Escherichia coli (E. coli), the additional demand for resources, such as nucleotides, tRNAs, ribosomes, and RNA polymerase (RNAP), may lower cell fitness by, for instance, affecting the growth rate of the cell (4–9). Furthermore, overexpressing one gene reduces the availability of resources and, as a consequence, decreases expression of other genes (10). This couples the expression of genes that do not have a direct regulatory link between them. These studies suggest that the cellular economy of gene expression, understood as the distribution of limited cellular resources to different genes, plays an important role in the behavior of genetic circuits.

Among the cellular resources required for gene expression, RNA polymerase and ribosomes are determining factors. Accordingly, studies have focused on how RNAP and ribosomes are distributed depending on the growth rate, used as a general descriptor of the status of the cell (6,8). Experiments performed by changing DNA concentration demonstrated that transcription is limited by the available amount of RNAP (11). Similarly, it has been shown that the availability of ribosomes is the major limiting factor in the translation process and one of the reasons why mRNA levels often do not correlate with the concentration of proteins produced in the cell (10). These findings indicate that RNAP and ribosomes are key transcriptional and translational resources that determine the cellular economy of gene expression. Therefore, characterizing how the products of different genes become coupled because of sharing limited amounts of ribosomes and RNAP is essential both for understanding the behavior of natural circuits and for engineering new ones.

In this article, we assembled a system with two fluorescent reporter proteins, one inducible (red fluorescent protein (RFP)) and one constitutive (green fluorescent protein (GFP)) without a regulatory path between them on the same plasmid, for several combinations of plasmid copy number and ribosome binding site (RBS) strength for the inducible gene (Fig. 1 A). Combining experiments on synthetic constructs with a mechanistic model, we discover that the coupling between two gene products located on the same plasmid but without a regulatory link between
them is captured by a linear relationship. This relationship can be interpreted as an isocost line, already employed in microeconomics to describe how two products can be purchased with a limited budget (12). This isocost line explicitly indicates how the extent of coupling depends on relevant parameters, such as RBS strength and plasmid copy number, and provides a simple tool to optimize circuits such that the extent of coupling is minimized.

MATERIALS AND METHODS

Bacterial strains, cell culturing, and fluorescence determination

Standard molecular biology techniques were used to prepare the different constructions in E. coli DH5α (see Sections A1 and A2 in the Supporting Material for details). All experiments were performed using the different allele (DIAL) strains harboring the cassette JTK160 in E. coli MC1061 (13). Growth conditions were selected to maximize the antagonistic effect of the inducible reporter on the constitutive. Preparing cultures coming from isolated colonies in LB plates were grown in 24-well plates using 1 ml of M9 minimal medium supplemented with 0.4% glucose, 0.2% casamino acids, 1 mM thiamine, ampicillin (100 μg/ml), and kanamycin (50 μg/ml). Cells were incubated for 8 to 10 h at 30°C and 100 rpm in an orbital shaker. When they reached the midlog phase, they were diluted (1/200) into 1 ml of the same M9 fresh media and incubated under the same conditions. Four hours after dilution, during exponential growth, the cultures were induced with N-acyl homoserine lactone (AHL; Cayman Chemical, Ann Arbor, MI) at a final concentration of 1, 2, 4, 10, and 1000 nM, and cells were grown for an additional 8 h until they reached the steady state of protein production, still in the exponential phase of growth. Unless explicitly stated (see Figs. S6–S8), the cultures were not induced with aTc.

For single-cell analysis, 5 to 10 μl aliquots were taken from each well every 1 h. The volume of the culture was kept constant replenishing with the same volume of fresh medium. Right after removal, the aliquots were diluted in 100 μl of water and analyzed in a BD Accuri C6 flow cytometer (BD Biosciences, San Jose, CA). The instrument is equipped with blue (488 nm) and yellow-green lasers (552 nm) for GFP and RFP, respectively. Emission was detected using a 525/50 filter for GFP and a 610/20 filter for RFP. Flow rates were always kept below 1000 events/sec and 30,000 to 100,000 events were analyzed in each read. Daily calibrations of the flow cytometer were performed using Spherotech 6 peak validation beads (BD Biosciences). To track the behavior of the whole population present in each well, the same plate was monitored every 20 min for absorbance (600 nm) in a Synergy MX (Biotek, Winooski, VT) plate reader.

Mathematical model

Module 1 in Fig. 1 A consists of a single gene expressing protein p1 (RFP) upon induction by the active transcription factor u (LuxR-AHL complex). In particular, promoter complex b1 is formed by u binding to the empty promoter b0 of the gene encoding p1, so that the binding of RNAP x can form the transcriptionally active promoter complex c1, resulting in the production of mRNA m1 encoding p1 at rate γ1 (encompassing the elongation reactions), which further decays at rate δ1:

\[
\begin{align*}
  &u + b_1^{b0} \xrightarrow{\mu_x} b_1, \quad b_1 + x \xrightarrow{\kappa_1} c_1, \\
  &c_1 \xrightarrow{\gamma_1} b_1 + x + m_1, \quad m_1 \xrightarrow{\delta_1} 0.
\end{align*}
\]

Translation of p1 is initialized by the ribosome y binding to the RBS of the mRNA m1, forming the translationally active complex d1. Protein p1 is degraded at rate λ1, whereas elongation and production are lumped together in one step with effective production rate π1:

\[
\begin{align*}
  m_1 + y \xrightarrow{k_1^+} d_1 \xrightarrow{\delta_1} y, \quad d_1 \xrightarrow{\pi_1} m_1 + y + p_1, \quad p_1 \xrightarrow{\lambda_1} 0.
\end{align*}
\]

Module 2 in Fig. 1 A consists of a single gene expressing protein p2 constitutively, that is, the production of p2 can be described with the following reactions:

\[
\begin{align*}
  b_2 + x \xrightarrow{k_2^+} c_2, \quad c_2 \xrightarrow{\gamma_2} b_2 + x + m_2, \quad m_2 \xrightarrow{\delta_2} 0, \\
  m_2 + y \xrightarrow{k_2^+} d_2 \xrightarrow{\delta_2} y, \quad d_2 \xrightarrow{\pi_2} m_2 + y + p_2, \quad p_2 \xrightarrow{\lambda_2} 0.
\end{align*}
\]

Because the total concentration of DNA is constant (14), we further have the conservation laws n = b1 + c1 = b2 + c2, where n is the plasmid copy number.

The experimental data presented in Fig. 1 B demonstrates that although the expression of a gene (gapA) affects that of another gene on the same plasmid (RFP), it has no effect on the steady-state expression of a third gene located on the chromosome (GFP), for details, see Figs. S2–S8. This indicates a separation between the resources available to the genes on the plasmid and those available to the chromosomal genes. To appropriately capture this by the model, we let X and Y represent the concentration of RNAP and ribosomes, respectively, available to the genes on the plasmid. We then write the conservation laws X = x + c1 + c2 and Y = y + d1 + d2, where x and y denote the free concentrations of RNAP and ribosomes, respectively, whereas c1 and d1 represent the concentration of RNAP and ribosome bound in module i (i = 1, 2). The separation of resources is not required for the existence of the isocost line and it only affects the extent of coupling between the expression levels of the two genes. Section B in the Supporting Material contains the details on the model and on the mathematical derivations leading to the isocost line, together with the simulation results.

RESULTS

Rationale of the circuit

We created a set of circuits that encode the expression of fluorescent reporters GFP and RFP to study how expression of one gene (RFP) affects that of the other (GFP) in E. coli cells (MBP-1.0; Fig. 1 A). GFP is produced constitutively whereas RFP is expressed only in response to AHL input, which binds the transcriptional activator LuxR. Each gene is encoded as an independent transcriptional module isolated from the others with double terminators. The plasmid also contains a ColE2-type origin of replication regulated by the RepA protein encoded in the bacterial chromosome. This enables us to dynamically control the plasmid copy number using the DIAL system of hosts (13). For a detailed description of the circuit and its components, see Fig. S1.

In a typical time course experiment we track, using flow cytometry, the expression of both reporters in cells growing in glucose 0.4% as the sole carbon source. Cells are kept in the exponential phase for the complete duration of the experiment from AHL induction and until the steady state
of protein production is reached (see Materials and Methods). By monitoring the population at the single-cell level we confirmed the absence of subpopulations of mutants not expressing the fluorescent genes that could interfere with our observations. Under these conditions, the circuit initially expresses GFP and LuxR. Induction with AHL results in an increase in the concentration of RFP while the concentration of GFP should in principle remain constant. However, we observe experimentally that as the concentration of RFP increases, the concentration of GFP decreases (Fig. 1A).

Experiments with both genes on the same plasmid allow us to rule out competition for factors involved in DNA replication, which may affect the relative abundance of reporters placed in separate replicons. We considered several alternative reasons beyond competition for cellular resources that could explain our observation, but all of them were discarded by control experiments as explained in what follows.

First, we focused on the two reporter genes used in this study, GFP and RFP. We checked possible effects on GFP fluorescence emission that could be affected by RFP excitation. We compared the fluorescence emission spectrum for the GFP channel of control cells containing or lacking RFP and the results are identical (Fig. S9). Furthermore, we swapped the two reporter genes (Fig. S10) and observed the same phenomenon as in Fig. 1A (for details, see Figs. S11–S14), leading to the conclusion that the results are not due to the fluorophore choice.

Second, we constructed MBP-chrom depicted in Fig. 1B by modifying MBP-1.0 (Fig. 1A) such that it contains genes encoding RFP and glyceraldehyde 3-phosphate dehydrogenase (gapA; accession no. NC_000913.2) in place of GFP and RFP, respectively. GapA is one of the most abundant endogenous proteins in the cytoplasm of *E. coli* growing on glucose (15) because it catalyzes one of the key steps of glycolysis, the conversion of glyceraldehyde 3-phosphate into 1,3-biphosphoglycerate (16). Furthermore, we inserted the Ptet-GFP cassette of MBP-1.0 (Fig. 1A) into the chromosome. Although the expression of GapA decreases that of RFP expressed from the same plasmid, it does not affect the expression of GFP integrated into the chromosome (Fig. 1B). This indicates that the pools of RNAP and ribosomes available to the genes on the plasmid are essentially separated from those available to the chromosomal genes.

Finally, we built two control circuits, MBP-gapA and MBP-dRFP (Fig. 1C), by modifying MBP-1.0 (Fig. 1A): MBP-gapA contains a gene encoding GapA in place of RFP, whereas MBP-dRFP lacks the RFP gene. We examined...
the production of GFP and RFP for circuits MBP-1.0, MBP-gapA, and MBP-dRFP in assays using different concentrations of inducer AHL. Induction of GapA with AHL has the same effect on GFP as inducing RFP, decreasing GFP production by up to 60% (Fig. 1C). This indicates that the GFP decrease is not because of the product RFP itself but rather to the process that produces RFP. Synthesis of GFP is not affected in the MBP-dRFP control, where RFP is not produced, indicating that it is not the transcriptionally active complex AHL-LuxR that has direct effect on GFP but it is the gene expression process induced by this complex that affects GFP (for details, see Figs. S15–S17). Taken together, the above results indicate that the decrease in GFP production upon RFP induction in MBP-1.0 (Fig. 1A) is because of the competition for RNAP and ribosomes caused by the production of RFP and not by the product RFP itself.

**Isocost lines describe the allocation of limited cellular resources**

We considered a mechanistic model of the synthetic circuit of Fig. 1A to understand how limited amounts of RNAP and ribosomes yield the experimental results in Fig. 1A (for details, see Materials and Methods and Section B in the Supporting Material). Using this model, we characterize the effect that module 1 producing p1 (RFP) has on p2 (GFP) in module 2. Specifically, we determine how this effect depends on the dissociation constant $k_1$ of the RBS of $p_1$ and on the plasmid copy number $n$. The concentration of available RNAP and ribosomes is denoted by $X$ and $Y$, respectively.

By analyzing this model, we obtain that the attainable output $(p_1, p_2)$ of the synthetic circuit in Fig. 1A satisfies the following formula:

$$\alpha p_1 + \beta p_2 = Y,$$

where $\alpha$ and $\beta$ are lumped constants incorporating the system parameters (for details, see Section B3 in the Supporting Material). The linear constraint in Eq. 1 can be interpreted as follows. With the available budget $Y$ of ribosomes, the cell can produce $p_1$ units of $p_1$ at price $\alpha$ and $p_2$ units of $p_2$ at price $\beta$. When $p_1$ is uninduced, the pair $(p_1, p_2)$ lies on the $p_2$-axis ($p_1 = 0$), and as we increase the level of induction of $p_1$, we move along a line from left to right (dark line in Fig. 2), increasing $p_1$ and simultaneously, decreasing $p_2$, according to Eq. 1. Using the conceptual analogy with microeconomics (12), we can interpret Eq. 1 as an isocost line.

The prices $\alpha$ and $\beta$ of $p_1$ and $p_2$ increase with the dissociation constants $k_1$ and $k_2$, respectively (see Section B3 in the Supporting Material), where $k_i$ is the dissociation constant of the ribosome binding to the RBS of the $p_i$. That is, the price of $p_1$ decreases by increasing the strength of the corresponding RBS. Therefore, the isocost line rotates clockwise by decreasing the RBS strength of $p_1$ (Fig. 2A). Hence, producing an extra molecule of $p_1$ leads to a larger effect on the concentration of $p_2$. This seemingly counterintuitive fact can be explained as follows. To attain the same protein concentration $p_1$ with a weaker RBS for $p_1$ (greater $k_1$) requires more mRNA, thus an increased usage of RNAP, and the same usage of ribosomes (see Section B3 in the Supporting Material). Consequently, less RNAP is available for the production of $p_2$, which, with the same amount of available ribosomes, leads to a smaller value of $p_2$. This, in turn, implies a steeper isocost line.

The plasmid copy number $n$ enters Eq. 1 via $\beta$ as it decreases with $n$ (see Section B3 in the Supporting Material). Hence, the price $\beta$ of $p_2$ increases as the plasmid copy number $n$ decreases, because more ribosomes are required to produce the same amount of $p_2$ (because of decreased mRNA concentration). By contrast, the price $\alpha$ of $p_1$ does not depend on the plasmid copy number $n$, because $p_1$ is inducible. In fact, the demand of $p_1$ for RNAP and ribosomes is determined by the concentration of induced $p_1$ promoter, which depends on two factors: the plasmid copy number $n$ and the concentration of the inducer of $p_1$. Low copy number and high induction results in the same demand for RNAP and ribosomes as high copy number and low induction (so that the concentration of induced promoters are equal). Production of an extra molecule of $p_1$ thus requires the reallocation of the same amount of resources, so that the price of $p_1$ is independent of $n$. Referring to Eq. 1, because $\beta$ decreases with $n$ and $\alpha$ is independent of $n$, a fixed $p_1$ allows more $p_2$ for a greater $n$. As a result, the isocost line shifts downward by decreasing the plasmid copy number $n$ (Fig. 2B).

The prices $\alpha$ and $\beta$ of $p_1$ and $p_2$, respectively, decrease as the total concentration $X$ of RNAP increases, so that the same budget $Y$ allows the production of more $p_1$ and $p_2$ (as a result of increased mRNA concentration). Similarly, keeping the prices $\alpha$ and $\beta$ fixed and increasing the budget $Y$ yields more $p_1$ and $p_2$ (as a result of increased ribosome concentration).

**Experimental validation of isocost lines**

We validated the theoretical predictions in experiments where either the RBS of RFP (Fig. 3) or the copy number
of the circuit were modified (Fig. 4). We therefore created a set of circuits with progressively weaker RBS strength for the RFP gene using a set of RBS sequences that range from very strong (MBP-1.0) to very weak undetectable translation of RFP (MBP-0.006) (see Table S3, for sequences, nominal, predicted, and observed strength values of the RBSs tested). The dose response curves show that weaker RBS strengths have reduced effects on GFP, with no appreciable effect in the case of MBP-0.006 (Fig. 3 A; for details, see Fig. S18). This experimental observation correlates well with numerical simulations of the model, which accounts for the conservation of ribosomes and RNAP along
with the usual production and degradation of RNAs and proteins (Figs. 3 and 28). The parameters used in the model were obtained from the literature (see Tables S4 and S5, for details). When plotting GFP over RFP we observe, as predicted by the isocost line (Eq. 1), a linear relationship between RFP and GFP productions (Fig. 3 B). Further, when the RBS of RFP becomes weaker, we observe that the slope becomes steeper (Fig. 3 B). This is in agreement with the prediction based on the isocost line (Eq. 1). In the experimental isocost lines, the intercept is higher for weaker RBSs of RFP. Further inspection revealed that there is production of RFP in the absence of AHL (Fig. S21) because of a basal level of transcription from Plux. Because of the coupling, circuits with stronger RBSs for RFP have lower initial values for GFP in the absence of AHL.

In addition to the original copy number of the plasmid MBP-1.0, we analyzed two lower plasmid copy numbers. Instead of replacing the origin of replication, which may in turn generate artifacts because of the involvement of different replication machinery for each of the origins, we used the DIAL host (13). For these experiments we always used the original MBP-1.0 construct but changed the DIAL host, to tune the number of copies of the circuit. The nominal exponential phase plasmid copy numbers were 64 ± 2 (J, medium), 18 ± 4 (I, low) and 4 ± 1 (E, very low) according to Kittleson et al. (13). The results in Fig. 4 A show that the decrease in GFP production depends on the number of copies of the plasmid and the corresponding percentage change is 48% and 29% for low and very low copy numbers, respectively (for details, see Fig. S23). Numerical simulations are consistent with the experimental data (Figs. 4 and S29). The parameters used in the model were obtained from the literature (see Tables S4 and S5, for details). When plotting the production of GFP as a function of RFP, we observe that the isocost lines shift down as the copy number decreases in agreement with the theoretical predictions (Fig. 4 B).

**Realizable region and minimizing circuit coupling**

Using the isocost lines, we next investigate how to design module 1 in Fig. 1 A so that when induced, its effects on module 2 are minimized. Specifically: How to choose the plasmid copy number \( n \) and the dissociation constant \( k_1 \) of the RBS of \( p_1 \) so that we minimize the sensitivity of \( p_2 \) to \( p_1 \), such that \((p_1, p_2)\) is fixed?

The design constraints are as follows. The plasmid copy number can vary between zero and its maximal value \( N \). Similarly, the RBS strength of \( p_1 \) varies between zero and its maximal value, so that the corresponding dissociation constant is between a minimal value denoted by \( K \) and infinity. Consequently, we call \( D = [0, N] \times [K, \infty] \) the design space. With this, it can be shown that the pairs \((p_1, p_2)\) that are realizable belong to the triangle \( \mathcal{R} \) defined by the origin and by the isocost line corresponding to \((N, K)\), depicted in Fig. 5, matching the experimental data. For details, see Section B5 in the Supporting Material.

The sensitivity of \( p_2 \) to \( p_1 \) is given by \( \Delta p_2 / \Delta p_1 = \alpha / \beta \). This can be minimized by decreasing \( \alpha \) and/or increasing \( \beta \). The price \( \alpha \) of \( p_1 \) can be minimized by picking \( k_1 = K \), corresponding to the strongest RBS for \( p_1 \). The value of \( \beta \) can be increased by decreasing the plasmid copy number \( n \). Because smaller \( k_1 \) requires smaller \( n \) to attain the same \((p_1, p_2)\) (see Section B5.2 in the Supporting Material), the sensitivity is minimized for the strongest RBS for \( p_1 \) and the corresponding plasmid copy number that attains the desired protein concentration \((p_1, p_2)\).

**DISCUSSION**

In this study, we have characterized the extent by which the products of different genes expressed from the same plasmid become coupled because of the limited availability of RNAP and ribosomes. This is a standard configuration used in the design of synthetic circuits that allows easy incorporation of modules to perform increasingly complex tasks. The extent of this coupling is substantial ranging from 60% when circuits are on medium copy number plasmids to 29% when circuits are on very low copy number plasmids. These effects can therefore be significant in the design of synthetic circuits even when assembled on low copy number plasmids. We discovered that this coupling is described by isocost lines, identifying quantities in the cellular economy of gene expression that play the same role as price and budget in microeconomics (12). The isocost line stems from the limited availability of RNAP and ribosomes in the transcription and translation processes. Although the existence of the
isocost line is not dependent on separation of resource pools between plasmid and chromosome, the slope of the line may be affected by this separation (see Section B3 in the Supporting Material). Our results (Fig. 1, A and B) indicate that the local depletion of resources plays a role in the extent of the coupling among gene expression levels; however, investigating how spatial proximity affects the extent of this coupling is beyond the scope of this work. Further studies considering either genes expressed from different plasmids or different locations on the same plasmid may provide additional information on how the extent of the coupling changes with spatial proximity.

Although it has been observed that gratuitous protein expression affects host growth (17), it has also been shown that such effects are largely dependent on the protein expressed, the copy number, and the culture conditions such as the nutritional quality of the carbon source used (19–21). In particular, previous experiments performed in conditions similar to ours showed that these effects are only transient in the exponential phase and that they disappear after several generations of exponential growth (22). We performed all our experiments with very low (3 to 5), low (14 to 22), and medium (62 to 66) plasmid copy numbers, lower than the numbers commonly considered in previous works. Furthermore, we performed all our measurements at steady state after several generations of exponential growth. This combination of factors contributes to the rather modest change in growth rate that we have observed in our experiments upon AHL induction (Figs. S22 and S27).

The study of the isocost line also sheds light on the role that RNAP and ribosomes each play in the coupling of gene expression. When using an extremely weak RBS for the inducible gene (RFP), we do not observe a significant decrease in the expression of the other gene (GFP). This result indicates that the decrease in GFP is mostly attributable to the limited availability of ribosomes, in accordance with what was observed in studies in vitro (23). However, the increase in slope of the isocost line when the RBS strength for RFP is decreased (Fig. 3 A) cannot be predicted unless RNAP is limiting (for details, see Section B6 in the Supporting Material). Our experimental results combined with our model indicate that the limited availability of RNAP manifests itself in a very subtle way. Specifically, a stronger RBS will allow a lower induction level to reach the same protein concentration. Lower induction, in turn, leads to lower demand for RNAP, which will then be available in higher concentrations to other genes, increasing their expression. This phenomenon, in which the limitation of RNAP plays a central role, controls the rotation of the isocost line.

Previous theoretical studies have analyzed how competition for common resources can affect the behavior of specific networks (24–26). In particular, Cookson et al. (24) modeled the sharing of common degradation machinery by multiple proteins and validated experimentally how this can alter the dynamic performance of synthetic circuits. Experimental demonstration of how this effect can be exploited to synchronize synthetic genetic oscillators was further demonstrated in Prindle et al. (27). Mather et al. (25) proposed a stochastic model to capture the anticorrelation between protein counts because of mRNAs competing for ribosomes. Rondelez (26) modeled enzymatic networks in which multiple substrates compete for the same enzyme and illustrated the dynamic effects of this competition on a synthetic oscillator called the metabolator. Except for the work of Cookson et al. and Prindle et al. (24,27), which studied competition for proteases as opposed to competition for RNAP and ribosomes, all the above works are purely theoretical and focus on modeling a specific system in which a species is competed for. By contrast, we provide experimental results on a set of synthetic constructs especially designed to validate a general model prediction about both the extent of coupling among genes because of competition for RNAP and ribosomes and the key parameters that control this coupling. The analogy that we have established with economics is not exclusive to how transcriptional and translational resources are distributed in the process of gene expression. Metabolism itself has been viewed as a market with supply and demand blocks that share products (28). At a higher level, it has also been proposed that biological regulatory systems seek high performance while trying to be economical (29,30).

Isocost lines will allow a deeper understanding of nontrivial interactions arising in natural systems, while being a step forward to the rational design of synthetic circuits. In particular, isocost lines establish a predictive framework for determining how circuit behavior is affected by competition for limited cellular resources and can be used as guidance for design.

SUPPORTING MATERIAL
Supporting Materials and Methods, Supporting Results, 31 figures, five tables, and MatLab data are available at http://www.biophysj.org/biophysj/supplemental/S0006-3495(15)00617-7.

AUTHOR CONTRIBUTIONS
D.D.V., R.W., A.G., J.J., and H.C. designed the research; D.D.V. and A.G. developed mathematical model; A.G. performed simulations; A.G., J.J., and H.C. performed experiments; J.Y., J.J., and H.-H.H. cloned constructs; D.D.V., R.W., J.J., and A.G. analyzed the data; and D.D.V., A.G. and J.J. wrote the article.

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SUPPORTING CITATIONS
References (31–45) appear in the Supporting Material.
