Observation of an anomalous Hall effect in single-crystal Mn$_3$Pt

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Abstract

The Mn$_3$X family of compounds was the first in which a large anomalous Hall effect (AHE) was predicted to arise from a purely antiferromagnetic structure, due to the Berry curvature in momentum space. Nearly simultaneously with this prediction, a large AHE was observed experimentally in one of the hexagonal members of this family, Mn$_3$Sn. Aligning antiferromagnetic domains, a necessary step for observation of the AHE, is more challenging for the cubic members of the Mn$_3$X family, due to a combination of smaller spontaneous ferromagnetic moments and much stronger magnetic anisotropy. Here, we use a combination of uniaxial stress and applied magnetic field to align domains of bulk single-crystal Mn$_3$Pt, and demonstrate for the first time a substantial AHE in a bulk sample of a cubic member of the Mn$_3$X family. The AHE remains locked in with essentially no quantitative variation when the stress is ramped back to zero, which shows that it is not a consequence of any stress-induced ferromagnetic moment.

1. Introduction

The anomalous Hall effect (AHE) was long thought to be a direct consequence of the magnetisation $M$ generated by ferromagnets [1]. However, in studies of the ferromagnet SrRuO$_3$, the anomalous Hall conductivity $\sigma_{xy}$ was found to have a nonmonotonic dependence on $M$ [2], and instead was found to be explainable as an integral of the spin Berry curvature in momentum space, following the proposal of Karplus and Luttinger [3]. This Berry phase mechanism is now understood to be the dominant mechanism for the intrinsic AHE [4]. One feature of this mechanism is that even antiferromagnets can generate a large AHE, as predicted, for example, for antiferromagnetism on a distorted fcc lattice [5], and observed experimentally in Pr$_2$Ir$_2$O$_7$ [6]. A large AHE is also predicted for the Mn$_3$X family of compounds [7, 8], which are antiferromagnetic. It has been demonstrated experimentally in bulk, single-crystal Mn$_3$Sn [9, 10], Mn$_3$Ge [11, 12], and Mn$_3$Ga [13]. A large, antiferromagnetically-induced AHE is a potentially valuable discovery for memory applications [14, 15].

These latter three compounds are all hexagonal. Other members of the Mn$_3$X family—Mn$_3$Pt, Mn$_3$Ir, and Mn$_3$Rh—are cubic. The cubic compounds are also expected to have large AHEs, but so far this has not been demonstrated in bulk single crystals. To observe the AHE in these compounds the magnetic structure must be trained, meaning that a subset of the possible antiferromagnetic domains must be selected, so that the AHE generated by individual domains does not cancel. It is easier to do so for the hexagonal compounds because they have an inverse-triangular spin configuration [16], within which the spins do not point in crystallographically equivalent directions. One consequence is that spin canting results in a net ferromagnetic moment, 3 $m_{\text{B}}$/Mn in Mn$_3$Sn and 7 $m_{\text{B}}$/Mn in Mn$_3$Ge, upon which applied magnetic field can act to select domains. Another is that the coercive field for domain re-orientation is low. The cubic compounds, on the other hand, have a triangular spin configuration in which the spins do point in
Figure 1. Unit cell of Mn₃Pt, showing the magnetic structure for $T < T_c \approx 400$ K. The Mn sites are numbered for reference. The curved arrows show the expected spin rotation when the lattice is compressed along the [001] axis, under an assumption of in-plane spin rotation. (a) Illustration of the A phase with the (111) spin plane. (b) Illustration of the B phase with the (111) spin plane. (c) A view of the magnetic structure along the [111] axis.

Stress-driven spin canting has been observed for Mn₃Sn [30]. For thin films of Mn₃Pt and Mn₃Ir, the observed AHE was of the same order as theoretical predictions developed for bulk lattices [31]. However, observations might be substantially affected by interface effects and disorder, and for this reason it is important to observe the AHE in bulk single crystals.

Here, we report a large, hysteretic AHE in bulk single-crystal Mn₃Pt, using a combination of applied field and uniaxial stress to train the magnetic structure. We study Mn₃Pt rather than Mn₃Ir because the ductile nature of Mn₃Ir makes it difficult to apply uniaxial stress. The AHE appears as a stress-induced field hysteresis in the Hall effect. The AHE remains locked in when the stress is released, which shows that stress-induced magnetism is not itself the source of the AHE, in agreement with the expectation that it is the antiferromagnetic structure that generates the AHE.

2. Methods

Single crystals of L₁₂–Mn₃Pt were grown by the Bridgeman–Stockbarger method [32]. All samples studied here were cut from the same original crystal. Resistivity data from two samples are shown in figure 2. The resistivity at 300 K is $65 \pm 3 \mu \Omega \cdot \text{cm}$, far smaller than the $175 \mu \Omega \cdot \text{cm}$ measured for the epitaxial films of [26].

Stress was applied using a piezoelectric-based uniaxial stress cell that incorporates sensors of both the force and displacement applied to the sample [33]. To allow in situ calibration of the zero-stress point, samples were mounted onto carriers that allowed application of compressive but not tensile stress. Three different, though conceptually equivalent, designs were used; one is shown in figure 3(a). It comprises two parts, and force is applied to the sample when they are brought together.

Samples 1, 2, and 3 had a longitudinal configuration: compression along [001] and $\mathbf{H} \parallel [001]$. Qualitatively, this configuration matches that of the thin film study of [26], in which the epitaxial strain yielded $a > c$, where $a$ is the lattice constant along [100] and [010]. This configuration obliges us to adopt a non-optimal contact configuration for measurement of the Hall resistivity: as shown in figures 3(b)–(d), current must be applied across the sample width. In a conventional configuration, the Hall voltage is:

$$V_y = \rho_{xy} I_x / t,$$

where $t$ is the sample thickness, perpendicular to the current direction, and in this configuration it is unclear what value is appropriate. $ho_{xy} = R_H B + \rho_{AHE} + \rho_{\text{offset}}$, where $R_H$ is the Hall coefficient, $\rho_{AHE}$ the anomalous Hall resistivity, and $\rho_{\text{offset}}$ is an offset due to misalignment of contacts. For samples 1–3, we applied equation (1) to
Figure 2. Temperature dependence of the resistivity of two samples of Mn$_3$Pt, at zero stress. The black lines are third-order polynomial fits, used later to calculate the Hall conductivity. The error bars indicate systematic uncertainty due to error in the placement of contacts.

Figure 3. Experimental setup. (a) Illustration of the sample carrier used for samples 1 and 4. The carrier is mounted onto a piezoelectric-driven cell that controls the distance between the pairs of anchor points. (b) Photograph of sample 1. (c) Schematic of the configuration for samples 1 and 3. The sample is held with epoxy between surfaces of the sample carrier, such that force is applied through the end faces of the sample. (d) Schematic of the configuration for sample 2. The ends of the sample are inserted into guides and secured with epoxy, such that force is applied to the sample dominantly through the side faces. The mounting epoxy for all samples was Stycast 2850FT, cured at 65°C for 180 minutes. (e) Applied force versus applied displacement for sample 4 at 100 K. The point labelled 'carrier contact point' is where the two parts of the carrier come into contact. The onset of plastic deformation is also indicated. The stress scale, on the right, is the stress applied to the sample.

obtain an effective thickness $t_{\text{eff}}$, so that $R_H$ at zero stress would match that measured in sample 4, which had a conventional Hall bar configuration. This $t_{\text{eff}}$ was then used to obtain the stress-driven changes in $\rho_{xy}$. Due to uncertainty in the true contact configuration, it is unlikely that more sophisticated analysis would yield better accuracy.

Sample 4 had a transverse configuration, with stress along [100] and $H \parallel [001]$, allowing a conventional contact configuration. A normal Hall coefficient of $R_H = -0.057 \, \mu\Omega\cdot\text{cm/T}$ was observed at 298 K. For comparison, $R_H$ of a 20 nm-thick film of Mn$_3$Pt in [26] was $-0.044 \, \mu\Omega\cdot\text{cm/T}$ at 365 K.

All stress values quoted in this paper are based on a room-temperature calibration of the force sensor of the stress cell, and are accurate to within 10%. The flexures of the sample carriers constitute springs placed in parallel with the samples; their total spring constant is 0.057 N \(\mu\text{m}^{-1}\) for the carrier illustrated in figure 3(a), and 0.023 N \(\mu\text{m}^{-1}\) and 0.020 N \(\mu\text{m}^{-1}\) for the other two designs. These spring constants are at most 5% of the spring constant of the sample system (see table 1), meaning that at least 95% of the applied force went into the sample rather than the carrier flexures.

Force-displacement data for sample 4 are shown in figure 3(e). There are two prominent features. One is the point where the two parts of the carrier come into contact, allowing force to be transmitted to the sample. Another is plastic deformation: the force-displacement relation transitioned to a shallower slope when the stress in this sample became larger than $-0.18$ GPa. (negative values denote compression.) As
There is no significant difference between them, which shows that any stress-induced ferromagnetic moment from data taken while holding the applied stress, and the red lines after the stress was ramped back to zero.

To a configuration like in figure 1(d), where the sample ends are deeply embedded in epoxy such that force is applied mostly through the side faces. For all samples, the field axis is the [001] direction.

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\text{Table 1. Key sample parameters. } k \text{ is the spring constant of the sample system, which is the sample itself in series with the mounting epoxy, and in parallel with the flexures of the sample carrier. } \sigma_{\text{plastic}} \text{ is the stress at which plastic deformation onset. Mount style A refers to a configuration like in figure 1(c), where force is applied dominantly through the sample’s end faces, and B to a configuration like figure 1(d), where the sample ends are deeply embedded in epoxy such that force is applied mostly through the side faces. For all samples, the field axis is the [001] direction.}
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| Sample # | Cross-section (mm\(^2\)) | Stress axis | \(k (\text{N } \mu\text{m}^{-1})\) | \(\sigma_{\text{plastic}}\) | Mount style |
|----------|----------------|-------------|----------------|-----------------|------------|
| 1        | 0.18 \(\times\) 0.18 | [001]       | 1.09            | -0.19 GPa at 300 K | A          |
| 2        | 0.40 \(\times\) 0.09 | [001]       | 1.09            | -0.20 GPa at 300 K | B          |
| 3        | 0.20 \(\times\) 0.20 | [001]       | 1.20            | -0.20 GPa at 100 K | A          |
| 4        | 0.30 \(\times\) 0.14 | [100]       | 0.97            | -0.18 GPa at 100 K | B          |

shown in table 1, plastic deformation began at a similar stress for all samples where it was observed, even at very different temperatures, and even for different mounting configurations (e.g., figures 3(c) and (d)) in which the stress field within the epoxy that holds the sample would have differed. We interpret this consistency, and the fact that with the same epoxy far higher stresses have been achieved in other materials [33], as showing that the plastic deformation occurred in the sample rather than the mounting epoxy. Evidently, the elastic limit of Mn\(_3\)Pt is much lower than that of Mn\(_3\)Sn, where elastic stresses larger than 1 GPa could be applied at temperatures near room temperature [34]. The experiment here was a constant battle with plastic deformation. We only report data taken in the elastic regime. Within the elastic limit and the maximum field in our measurement system, 12 T, we obtained clear magnetic hysteresis, but not complete polarisation of the domains.

3. Results

We begin with magnetometry measurements on unstressed samples, to investigate possible spontaneous ferromagnetism. As noted in the Introduction, the cubic symmetry of the lattice competes with nearest-neighbour antiferromagnetic interaction, and is expected to cause a small spin rotation out of the plane [17, 25]. For the domain illustrated in figure 1(a), the resulting net moment would point along the [111] or [111] direction. In Mn\(_3\)Ir, a net moment of 7 m\(\mu\)B/Mn has been predicted [7].

Mn\(_3\)Pt does not transition directly into the structure illustrated in figure 1(a), but rather passes through an intermediate phase between \(T_S \approx 400\) K and \(T_N \approx 475\) K with a collinear spin structure [35–37]. Data for \(H || [111]\) are shown in figures 4(a), (c) and (d), and for \(H || [100]\) in figures 4(b), (e) and (f). The samples were thermally cycled to 600 K, well above \(T_N\), and cooled in either 0 or 7 T. For both samples, a net polarisation of 0.3–0.4 m\(\mu\)B/Mn is visible below \(T_S\). This is a small net moment, and because it may include contributions from polarisation of spins in the vicinity of defects and magnetic domain walls, it should be understood as an upper limit on the intrinsic net moment.

We now discuss measurements of the Hall effect. \(\rho_{xy}\) data from sample 1 are shown in figure 5(a).

At zero stress (the blue curve), the field dependence of \(\rho_{xy}\) is dominated by the normal Hall effect. There is resolvable hysteresis, but it is small. Under an applied stress of \(-0.14\) GPa (thick red and black curves), the hysteresis became much larger. When the stress was released after application of a field of +12 T at \(-0.14\) GPa, the hysteresis loop closed up again, showing that the enhanced hysteresis was not a product of any non-elastic deformation. However, the new curve (the thin red curve) was offset from the original blue curve. Similarly, the zero-stress data recorded after application of \(-12\) T at \(-0.14\) GPa (the green curve) also showed small hysteresis, but were offset from the original curve in the other direction. Evidently, the hysteretic part of \(\rho_{xy}\) remains at least mostly locked in after the stress is released.

Figure 5(b) shows hysteresis loops with backgrounds subtracted; the background is taken as a quadratic function of \(\mu_0H\), obtained independently at each stress. Each hysteresis loop is recorded following this procedure: (a) under applied stress, \(B\) is ramped from 0 to +12 T, and then back to 0; (b) the stress is then released, to measure the Hall effect at zero applied stress; (c) the stress is re-applied, and \(B\) ramped from 0 to \(-12\) T, then to 0; (d) the stress is released again and the Hall effect re-measured. The 0 GPa readings are indicated by large squares; it is apparent that releasing the stress causes essentially no change in \(\rho_{xy}\).

Hysteresis loops for samples 2 and 3, though without the ramps back to 0 GPa, are shown in figure 5(c).

The anomalous Hall conductivity \(\sigma_{\text{AHE}} = -\rho_{xy}/\rho^2\) for samples 1 and 2 is shown in figure 6(a). \(\rho_{AHE}\) at each stress is taken as \(\frac{1}{2} (\rho_{xy}(H=0) - \rho_{xy}(H=0))\), where \(\rho_{xy}(H=0)\) is the Hall resistivity after application of \(\mu_0H = \pm 12\) T for sample 1 and \(\pm 10\) T for sample 2. \(\rho_{xx}\) is taken from sample 4, where the contact configuration permitted accurate measurement; see figure 2. The grey squares in figure 6(a) show \(\sigma_{xy}\) derived from data taken while holding the applied stress, and the red lines after the stress was ramped back to zero. There is no significant difference between them, which shows that any stress-induced ferromagnetic moment contributes negligibly to the AHE.
Figure 4. Magnetometry data on unstressed Mn$_3$Pt, setting an upper limit on the spontaneous magnetisation. (a) Magnetisation $M$ against temperature for sample 6 and $H$ applied along [111]. ‘ZFC’ indicates zero-field cooled, ‘FC’ field-cooled, under a 7 T applied field. (b) $M(T)$ for sample 7 and field along [100]. (c) $M(H)$ at 300 K for sample 6, after cooling from 600 K in either zero field or 7 T. Open points indicate increasing $H$, filled points decreasing $H$. (d) The data from (c), but with a linear fit to the ZFC data subtracted. (e) and (f) Equivalent to panels (c) and (d) for sample 7 and $H \parallel [100]$.

Figure 5. (a) Example raw data for sample 1. (b) Background-subtracted data for sample 1. Open points are for increasing $H$, filled points decreasing $H$. Under uniaxial stress, the hysteresis in $\rho_{xy}(H)$ expands. The large squares are $\rho_{xy}$ measured after the applied stress was ramped back to 0 GPa. For clarity, data at the separate stresses are offset by 0.2 $\mu\Omega$·cm. (c) Background-subtracted data for samples 2 and 3. Data from sample 2 are offset by 0.6 $\mu\Omega$·cm.
After a year-long pause, we attempted to achieve saturation of the AHE in sample 1 by driving it to higher compression. These data points are indicated by the X’s in figure 6(a). Their position is shifted by hand along the stress axis to match the earlier data set, compensating for relaxation in the mounting epoxy that occurred during the long pause. These data make clear that within the limits of our maximum field (12 T) and the elastic limit of the samples (~0.2 GPa) clear saturation could not be achieved, and it is not clear how much higher field and/or stress would be required. The coercive field for strained bulk Mn₃Pt is evidently far higher than that observed in the thin film study, where it was ~0.1 T [26]. Disorder and/or interface effects may have suppressed the coercive field in the thin films.

Separately, we note that in [26] the intrinsic AHE was calculated to have a strain dependence. According to this calculation, at the largest stress that we reached the anomalous Hall conductivity would be 4% lower than at zero stress. Such a change would be at the edge of our present sensitivity.

Figure 6(b) shows σ_{AHE} of sample 1 at various temperatures, after training the magnetic structure at 300 K with σ = −0.14 GPa and µ_BH = ±12 T. σ_{xy} increases steadily with cooling, as was observed with Mn$_3$Pt$_4$Ge$_6$ [12].

We now show, in figure 7, stress-induced hysteresis for sample 4, which was the one with a transverse configuration: compression along [100], H ∥ [001]. As for sample 1, for sample 4 there was discernible though small hysteresis at zero applied stress. Measurements at three different temperatures (100, 200, and 298 K), shown in figure 7(c), reveal a consistent effect of the applied stress: σ_{AHE} decreases under compression, a change of the opposite sign to that observed when σ ∥ [001]. However, the quantitative effect is much smaller than for σ ∥ [001].

4. Discussion and conclusion

We have shown that the AHE of Mn₃Pt can be trained by simultaneous application of uniaxial stress and field. In other words, uniaxial stress reduces the coercive field for reorientation of the antiferromagnetic domains. Stress that is longitudinal with respect to the field is more effective than transverse stress. In this section we discuss three possible mechanisms by which uniaxial stress might reduce the coercive field. (a) Piezomagnetism due to out-of-plane rotation of the spins (b) piezomagnetism due to in-plane rotation of the spins; and (c) approach to an alternative magnetic ground state.

Piezomagnetism is given by $M_i = \sum_{j,k} \Lambda_{ijk}\sigma_{jk}$, where $M$ is the induced magnetic moment, $\sigma$ is stress, and $\Lambda_{ijk}$ is the piezomagnetic tensor. For the magnetic space group of Mn₃Pt, R3m, $\Lambda_{zzz}$ and $\Lambda_{xxx}$ are both nonzero, though with different coefficients. This means that both $z$-axis and $x$-axis uniaxial stress can induce a $z$-axis magnetic moment. Due to concerns about plastic deformation we did not attempt to measure the piezomagnetism of Mn₃Pt. In the epitaxial thin film study of [26], a net magnetic moment of 4.6 m$_\mu_B$/Mn was obtained for a 20 nm-thick film with c/a = 0.990. For bulk samples, that ratio of c/a would be obtained under a uniaxial stress of $\sigma \approx -0.8$ GPa, indicating a piezomagnetic coefficient of $\approx 6$ (m$_\mu_B$/Mn)/GPa. At our largest stress of $\sigma \sim -0.2$ GPa, a piezomagnetic moment of 1.2 m$_\mu_B$/Mn would be obtained, well above

5 The bulk modulus of Mn₃Pt is 115 ± 8 GPa [39], and the Poisson's ratio is 0.35 [26], which together yield a Young's modulus of 106 ± 7 GPa.
our upper limit for the spontaneous magnetisation in unstressed Mn$_3$Pt. For comparison, 8 (m$\mu$/Mn)/GPa has been measured for in-plane stress applied to Mn$_3$Sn [30], and $\sim$100 (m$\mu$/Mn)/GPa has been reported for Mn$_3$NiN [38].

In the triangular state at $T < T_t$, there are eight equivalent domain types. There are four possible spin planes: (111), (111), (111), and (111), and for each there are two domain types, related by time reversal. Following [7], these can be classed as A-phases, where the spins point outward with respect to the triangle that is higher along [001], and B-phases, where they point inward—see figure 1 for an illustration. In the experimental geometry here, where our Hall effect measurements probe effective fields parallel to [001], the AHE from A and B phases will be opposite.

We discuss now the first of the possible mechanisms listed above: out-of-plane spin rotation. For each of the possible spin planes, the angle between the axis of the spin plane (line perpendicular to the spin plane) and the [100] and [001] directions is the same. This means that the out-of-plane rotation induced by [001] and [100] uniaxial stress should be nearly the same. Therefore, this form of piezomagnetism would not account for the differing effects of longitudinal versus transverse stress.

The second possible method, in-plane spin rotation, could explain the difference between longitudinal and transverse stress. The black arrows in figure 1 indicate the expected spin rotation under compression along [001] for the A and B phases, under an assumption of in-plane spin rotation. Spin 1 does not rotate because there is no symmetry breaking between clockwise and counter-clockwise rotation. Spins 2 and 3 rotate away from spin 1 because the bond length to spin 1 is reduced. That the magnetic interaction energy increases with reduced bond length is shown by the fact that $T_N$ under strong hydrostatic compression, where the collinear phase is suppressed and the transition at $T_N$ is directly into the triangular phase, increases with compression [39]. Measurements of spin waves show in addition that nearest-neighbour interaction is dominant [40]. For the A phase, the resulting net moment points along [112]. Compression along [100], on the other hand, would cause spins 1 and 3 to rotate, resulting in a net moment for the A phase along [111]. Its projection along [001] is opposite to that induced by [001] compression, and half as large. The same will be true for the other possible spin planes. Therefore, for a given field along [001], opposite domain types—A versus B—should be selected by longitudinal versus transverse stress, with transverse stress being less effective. We note that orbital polarisation could add comparably to, and even reverse, the net moment from spin rotation [41, 42], but this anisotropy remains. Thus, piezomagnetism from in-plane spin rotation could explain both the opposite sign and differing magnitudes of the AHE induced by [001] and [100] uniaxial stress, for $H \parallel [001]$.

The third possible mechanism, approach to an alternative magnetic ground state, is one for which we cannot provide specific evidence, but which is nevertheless possible. Stress along ⟨100⟩ directions is not aligned with the principal axes of the magnetic order or the local easy axes of the Mn spins, making it likely that the applied stress will eventually favour an alternative ground state. In other magnetic systems, stresses well below 1 GPa have been observed to qualitatively change the magnetic structure [43, 44]. There is evidence for closely-spaced ground states in Mn-based systems. In Mn$_3$GaN, a state where the spins are rotated by 90° with respect to the Mn$_3$Pt structure may be the ground state [45–47], and may be close to the ground state in Mn$_3$Pt [48]. In Mn$_3$Ge and Mn$_3$Ga there is a strong susceptibility for rotation of the spins.
out of the plane [49, 50]. Therefore, it is possible that the coercive field of Mn$_3$Pt weakens under uniaxial stress because magnetic anisotropy weakens as an alternative magnetic ground state is approached.

As in the thin film study, the AHE observed here is of the same order of magnitude as predicted theoretically [26, 31]. Without demonstration of saturation of the magnetic domains, we cannot offer detailed comments on the magnitude of $\rho_{\text{AHE}}$.

In conclusion, we have shown that uniaxial stress reduces the coercive field for training the magnetic structure of Mn$_3$Pt, allowing experimental observation, for the first time, of the AHE in bulk samples of a cubic member of the Mn$_3$X family. The AHE induced by stress and field remains locked in after the stress is released, which shows that the effect of any stress-induced ferromagnetic moment on the Hall effect is negligible. Longitudinal stress reduces the coercive field faster than transverse stress, an observation suggesting that in-plane spin rotation is the dominant response to the applied stress. This hypothesis is not the only possibility, and so should be tested through direct observation of the piezomagnetism. Saturation of the AHE may prove possible through combinations of stress and field directions not probed here, allowing precise comparison with calculations on single crystals, and we therefore encourage further experimentation.

**Data availability statement**

The data that support the findings of this study are available upon reasonable request from the authors.

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