Quantified Uncertainties in Comparative Life Cycle Assessment: What Can Be Concluded?

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ABSTRACT: Interpretation of comparative Life Cycle Assessment (LCA) results can be challenging in the presence of uncertainty. To aid in interpreting such results under the goal of any comparative LCA, we aim to provide guidance to practitioners by gaining insights into uncertainty-statistics methods (USMs). We review five USMs—discernibility analysis, impact category relevance, overlap area of probability distributions, null hypothesis significance testing (NHST), and modified NHST—and provide a common notation, terminology, and calculation platform. We further cross-compare all USMs by applying them to a case study on electric cars. USMs belong to a confirmatory or an exploratory statistics’ branch, each serving different purposes to practitioners. Results highlight that common uncertainties and the magnitude of differences per impact are key in offering reliable insights. Common uncertainties are particularly important as disregarding them can lead to incorrect recommendations. On the basis of these considerations, we recommend the modified NHST as a confirmatory USM. We also recommend discernibility analysis as an exploratory USM along with recommendations for its improvement, as it disregards the magnitude of the differences. While further research is necessary to support our conclusions, the results and supporting material provided can help LCA practitioners in delivering a more robust basis for decision-making.

INTRODUCTION

One of the main applications of life cycle assessment (LCA) is to support a comparative assertion regarding the relative environmental performance of one product with respect to other functionally equivalent alternatives.1 In such a comparative LCA, claims can be tested by comparing the inventory and/or impact assessment results for any given set of alternative products. To date, practitioners usually calculate and compare point-value results, an approach described as deterministic LCA. This practice allows one to draw conclusions such as “alternative B causes 45% larger impacts than alternative A” or “alternatives B and C have strengths and weaknesses, but both outperform alternative D.” Typically, deterministic comparative LCAs find trade-offs between alternatives and across environmental impacts (from here on referred to as impacts). While uncertainty estimations can be useful in understanding trade-offs between alternatives, deterministic LCAs lack an assessment of uncertainties.

Uncertainty appears in all phases of an LCA5−7 and originates from multiple sources. Some of the more prevalent are variability, imperfect measurements (inherent uncertainty), gaps, unrepresentativeness of inventory data (also known as parameter uncertainty),5 methodological choices made by practitioners throughout the LCA (also known as scenario uncertainty or uncertainty due to normative choices),6 and mathematical relationships (also known as model uncertainty).5 Using analytical and stochastic approaches, e.g., Monte Carlo (MC) simulations and first order Taylor series expansion,9 LCA practitioners have propagated these sources of uncertainty to LCA results.9,10 Unlike deterministic LCA, the quantification of uncertainties related to LCA results allows for associating a level of likelihood to and confidence in...
the conclusions drawn. However, interpreting overlapping ranges of results is complex and therefore requires sophisticated interpretation methods. To this end, various statistical methods have been applied within the field of LCA, including: discernibility analysis,\textsuperscript{11,12} impact category relevance,\textsuperscript{13} overlap area of probability distributions,\textsuperscript{14} null hypothesis significance testing (NHST),\textsuperscript{15,16} and modified NHST.\textsuperscript{17}

The application of statistical methods to uncertainty analysis results, hereafter referred to as “uncertainty-statistic methods” (USMs), can aid practitioners in various ways. First, they help to establish a level of confidence behind the trade-offs between alternatives and across environmental impacts while considering various sources of uncertainty. Second, they go beyond the practice of one-at-the-time scenario analysis by integrating a series of otherwise independent sensitivity analyses into an overall uncertainty assessment of results.\textsuperscript{5} For instance, they enable the exploration of a broad range of possible combinations of all sorts of input data known as the scenario space.\textsuperscript{12} Third, they allow for comparisons of alternatives in the context of common uncertainties, a crucial aspect in comparative LCAs.\textsuperscript{18} Lastly, they help to identify the relative importance of different impacts for the comparison of alternatives.\textsuperscript{18}

Choosing the most appropriate statistical method(s) to interpret the results of uncertainty analysis in the light of the goal and scope of individual LCA studies can be challenging. There is a lack of applications of these methods in real case studies, a lack of support in standard LCA software, in comprehensiveness and scattered documentation, and inconsistent terminology and mathematical notation. Moreover, literature is devoid of recommendations for LCA practitioners about which method(s) to use, under which LCA goal, to interpret the meaning of the uncertainty analysis results in comparative LCAs. Thus, our research question queries: “Which statistical method(s) should LCA practitioners use to interpret the results of a comparative LCA, under the light of its goal and scope, when considering uncertainty?” In this study, we answer this question by (1) critically reviewing the five above-mentioned USMs, (2) comparing them for a single illustrative case study on passenger vehicles with a common calculation platform and terminology, and (3) by providing guidance to practitioners in the realm of application of these methods via a decision tree. It is the focus of this study to test the applicability and value of different USMs, including the visualization of results and the limitations encountered during their implementation. Testing and analyzing differences in methods to quantify and propagate uncertainties is out of the scope of this study, although we use some of them (e.g., Monte Carlo simulations as propagation method) for the uncertainty analysis.

## METHODS AND CASE STUDY

### Statistical Methods for Interpretation of Comparative LCA with Uncertainty

In chronological order of publication, the methods we study are discernibility analysis,\textsuperscript{11,12} impact category relevance,\textsuperscript{13} overlap area of probability distributions,\textsuperscript{14} null hypothesis significance testing (NHST),\textsuperscript{15,16} and modified NHST.\textsuperscript{17} The scope was narrowed to these statistical methods for the comparison of alternatives.\textsuperscript{18}

The method has been developed and published in peer reviewed journals and contains transparent and accessible algorithms. Consequently, the first-order reliability method (FORM)\textsuperscript{3} could not be included due to incompletely documented optimization procedures.

(2) The method is applied to interpret the results of uncertainty analysis of comparative LCAs with two or more alternatives and one or more emissions or impacts. This excludes studies addressing different impacts, but not in a comparative way,\textsuperscript{19} and studies focusing on methods for quantifying and/or propagating uncertainty sources through LCA. Studies developing and describing methods such as global sensitivity analysis\textsuperscript{20} are also excluded as they are not comparative and focus on just one emission or impact at a time. Finally, we have not revisited the enormous body of statistical literature, as the authors of the selected methods have already done this exercise.

To increase transparency in our comparison of methods and their features, we use a uniform terminology (Table S.1, Appendix I of the Supporting Information, SI), and a common mathematical notation (Table 1). We interpret the state of the art for each method, and in some cases go beyond the original mathematical proposals by the authors. When this is the case, we indicate the differences.

We reviewed the methods according to the following aspects: the number of alternatives compared and approach to compare them, the inputs used by the method, the implementation, the purpose and the type of outputs. Table 2 summarizes the features of each method according to these aspects.

Some features that are consistent for all methods include: (1) they can be applied to dependently or independently sampled MC runs, meaning that the uncertainty analysis results are (dependently) or not (independently) calculated with the same technology and environmental matrices for all alternatives considered for each MC run; (2) they can be used to interpret LCA results at the inventory, characterization, and normalization level, although in our case study we only apply them at the characterization level as their use at other levels is trivial in the absence of additional uncertainties; (3) they all compare alternatives per pairs (pairwise analysis); and (4) they all originate from the idea of merging uncertainty and comparative analysis.

**Discernibility.** We refer to discernibility as the method described by Heijungs and Kleijn\textsuperscript{11} as the basis of comparative evaluation of Gregory et al.\textsuperscript{12} is the same as that proposed by...
The results of eq 1 help assert that “Alternative j has a larger impact than alternative k in 100 \times f \% of runs”.

**Impact Category Relevance.** This approach evaluates trade-offs using the relevance parameter \((Y_{ijk})\), as introduced in Prado-Lopez et al.,\(^{13}\) and it is not intended to calculate statistical significance. It stems from the idea that similar impacts among alternatives do not influence the comparison of alternatives as much as impacts for which alternatives perform very different. It uses the mean (statistics of centrality, \(\bar{X}_{ij}, X_{ij}\)) and standard deviation (statistic of dispersion, \(S_{ij}, S_{ik}\)) calculated from the obtained values for each impact \((X_{ijr} \text{ and } X_{ijk})\), thus not per MC run. The value of \(Y_{ijk}\) has no meaning on its own, rather its purpose is to help explore the comparison of two alternatives by means of sorting according to the extent of the differences per impact. This approach is therefore exclusive to analysis with more than one impact. When uncertainties increase (as indicated by larger standard deviations) or the difference between the means of two alternatives gets closer to zero (as indicated by nearly equal means), it becomes harder to distinguish between the performance of two alternatives for an environmental impact and hence this aspect is deemed to have a lower relevance in the comparison. A higher relevance parameter for a specific impact indicates that this impact is more important to the comparison than others. The relevance parameter works as a pairwise analysis, as shown in eq 2.

\[
Y_{ijk} = \frac{\bar{X}_{ij} - \bar{X}_{ik}}{\frac{1}{2}(S_{ij} + S_{ik})}
\]

(2)

In this formula we interpret (in comparison to the original description of the method\(^{13}\)) \(\mu_i\) as \(\bar{x}\), because \(\mu\) is unknown and only estimated by \(\bar{x}\). Further, we interpreted the ambiguous SD in the original publication,\(^{13}\) into \(s\), which is an estimate of \(\sigma\). **Overlap Area of Probability Distributions.** This method follows the same idea as the relevance parameter, but instead provides an indicator based on the overlap area of probability distribution functions (PDF). Similar to the relevance parameter, this method is not calculated per run, and there is no significance threshold value in the overlap that defines statistical significance. The overlap area approach is exclusive to analysis with more than one impact.\(^{14}\) It measures the common area between PDF of the stochastic impact results \((X_{ij} \text{ and } X_{ik})\) of two alternatives \(j\) and \(k\) for a specific impact \(i\). By doing this, the overlap area approach can technically apply to diverse types of distributions as opposed to assuming a normal distribution. The shared area between distributions ranges from one, when distributions are identical, to zero, when they are completely dissimilar. The smaller the overlap area, the more different two alternatives are in their performance for an impact. To compute the overlap area \((A_{ijk})\), two strategies can be followed. A conventional way is to assume a probability distribution for both \(X_{ij}\) and \(X_{ik}\) (for instance, a normal or log-normal distribution), to estimate the parameters \((\mu_{ij}, \mu_{ik}, \sigma_{ij}, \sigma_{ik})\) from the MC samples, and to find the overlap by integration. This is the approach followed by Prado-Lopez et al.,\(^{14}\) using log-normal

| Method                         | Alternatives compared (approach) | Type of input (from uncertainty analysis) | Implementation | Purpose (type of question) | Type of output | Reference |
|--------------------------------|----------------------------------|-------------------------------------------|----------------|-----------------------------|----------------|-----------|
| Deterministic LCA              | as many as required (all together) | none                                       | overall (i.e., based on one run or point-value) | which alternative displays the lower results? (exploratory) | point-value    | abundant in literature, included as standard result in LCA software packages Heijungs et al.\(^{11}\) |
| Discernibility                 | as many as required (pairwise analysis) | Monte Carlo runs (dependently or independently sampled) | per run | how often is the impact \(j\) higher for \(j\) than \(k\) or vice versa? (exploratory) | counts meeting "sign test" | Heijungs and Klein\(^{11}\) |
| Impact Category Relevance      | as many as required (pairwise analysis) | estimates of statistical parameters (i.e., mean and standard deviation) | overall (i.e., based on statistical parameters) | which are the impacts playing a relatively more important role in the comparison of \(j\) and \(k\)? (exploratory) | measure of influence of impacts in the comparison (eq 1) | Prado-Lopez et al.\(^{13}\) |
| Overlap Area of Probability Distributions | as many as required (pairwise analysis) | moments of the fitted distribution (e.g., maximum likelihood estimates) | overall (i.e., based on the fitted distribution) | which are the impacts playing a relatively more important role in the comparison of \(j\) and \(k\)? (exploratory) | overlap of probability distributions of \(j\) and \(k\) (eq 3) | Prado-Lopez et al.\(^{14}\) |
| Null Hypothesis Significance Testing (NHST) | as many as required (pairwise analysis) | Monte Carlo runs (dependently or independently sampled) | per run | is the mean impact of \(j\) significantly different from the mean impact of \(k\)? (confirmatory) | \(p\)-values fail to reject (no) or reject (yes) the null hypothesis | Henriksson et al.\(^{15}\) |
| Modified NHST                  | as many as required (pairwise analysis) | Monte Carlo runs (dependently or independently sampled) | per run | is the difference between the mean impact of \(j\) and \(k\) at least as different as a threshold? (confirmatory) | \(p\)-values fail to reject (no) or reject (yes) the null hypothesis | Heijungs et al.\(^{17}\) |
distributions. The second approach does not require an assumption on the distribution, but uses the information from the empirical histogram, using the Bhattacharyya coefficient. To our knowledge, the latter approach has not been used in the field of LCA. Here, we calculate the overlap area using the first approach. In our case, the statistic of centrality ($X_{ij}$, $X_{ik}$) and dispersion ($S_{ij}$, $S_{ik}$) of the assumed lognormally distributed stochastic impact results were calculated by means of the maximum likelihood estimation of parameters. The lower intercept ($\theta$) and the upper intercept ($\mu$) of the two PDFs, are calculated using these parameters and used as a base to calculate the overlap area between two distributions (eq 3). Details on the calculation of $\theta$ and $\mu$, as well as the maximum likelihood estimation of parameters $\mu$ and $\sigma$, and the PDF $\Phi$ are described in the SI (Appendix II).

$$A_{i,j,k} = 1 - |\Phi(\theta; \mu_{i,j}, \sigma_{i,j}) - \Phi(\theta; \mu_{i,k}, \sigma_{i,k})|$$

$$- |\Phi(\mu; \mu_{i,j}, \sigma_{i,j}) - \Phi(\mu; \mu_{i,k}, \sigma_{i,k})|$$

(3)

This method uses a pairwise analysis, yet when more than a pair of alternatives is compared, Prado-Lopez et al. proposed an averaging procedure for the overlap areas between all pairs. For reasons of comparability with the other methods, we did not pursue this extension and concentrate instead on the comparison per pair.

**Null Hypothesis Significance Test (NHST).** This method is delineated in Henriksson et al. and applied in Henriksson et al. It largely relies on established null hypothesis significance tests. In comparative LCAs, a generally implicit null hypothesis presumes that two alternatives perform environmentally equal: $H_0: \mu_{ij} = \mu_{ik}$. This method’s purpose is to show whether the centrality parameter (mean or median) of the relative impacts of two alternatives are statistically significantly different from each other. It builds on the quantification and propagation of overall dispersions in inventory data to stochastic LCA results ($X_{ij}$ and $X_{ik}$). From the stochastic results per impact, the difference per pair of alternatives per MC run is calculated ($X_{ij} - X_{ik}$). This distribution of differences can then be statistically tested using the most appropriate statistical test with regards to the nature of the data, as proposed by Henriksson et al. For instance, for normally distributed data, a paired $t$-test is appropriate to determine whether the mean of the distribution significantly differs from zero (the hypothesized mean). For non-paramaterized data, more robust statistical tests, such as Wilcoxon’s rank test, can be used. When three or more alternatives are compared, a two-way ANOVA can be used for normally distributed data, while a Friedman test can be used in more general cases. In both of these cases a posthoc analysis is also required to establish significantly superior products. The null hypothesis of equal means (or medians) may then be rejected or not, depending on the $p$-value and the predefined significance level ($\alpha$), e.g., $\alpha = 0.05$. For our case, we apply a paired $t$-test to the distribution of the difference per pair of alternatives and MC run, because the mean is expected to be normally distributed as the number of runs is relatively large (1000 MC runs). We also explored a Bonferroni correction of the significance value from $\alpha = 0.05$ to $\alpha_{ij} = 0.05/30 = 0.0016$ as the chance of false positives is rather high when multiple hypothesis tests are performed. The factor 30 is explained by the ten impacts and the three pairs of alternatives.

**Modified NHST.** Heijungs et al. proposed this method as a way to deal with one of the major limitations encountered while applying NHST to data from simulation models: significance tests will theoretically always reject the null hypothesis of equality of means since propagated sample sizes are theoretically infinite. It is a method that attempts to cover significance (precision) and effect of size (relevance). Thus, from the classic $H_0$ in NHST that assumes "no difference" between the parameters ($\mu_{ij} = \mu_{ik}$), this method includes a "at least as different as" in the null hypothesis, which is stated as $H_0: S_{ijk} \leq \delta_0$, where $S_{ijk}$ is the standardized difference of means (also known as Cohen’s $d$) and $\delta_0$ is a threshold value, conventionally set at 0.2. So far the method has not been applied in the context of comparative LCA outside of Heijungs et al. For its operationalization, the authors proposed the following steps: (1) set a significance level ($\alpha$); (2) set the difference threshold ($\delta_0$); (3) define a test statistic $D$ (see eq 4, which is a modification from the original proposal); and (4) test the null hypothesis $H_0$: $\delta \leq \delta_0$ at the significance level $\alpha$.

$$d_{i,j,k} = x_{ij} - x_{ik}$$

that estimates $\hat{\delta}_{ijk} = \frac{\mu_{ij} - \mu_{ik}}{\sigma_{i,j,k}}$

$$s_{i,j,k} = \sqrt{\frac{1}{N - 1} \sum_{i=1}^{N} (x_{ij} - x_{ik} - (x_{ij} - x_{ik}))^2}$$

(4)

In eq 4, $s_{i,j,k}$ is the standard deviation of the difference between alternatives $j$ and $k$. We further estimate the $t$-value from the value of $d$ as shown in eq 5. The $t$-value is a test statistic for $t$-tests that measures the difference between an observed sample statistic and its hypothesized population parameter in units of standard error.

$$t_{i,j,k} = \frac{d_{i,j,k} - \delta_0}{s_{i,j,k}}$$

(5)

For our case, we consider the default values suggested by Heijungs et al. where $\alpha = 0.05$ and $\delta_0 = 0.2$, and we calculate the test statistic $D$ for the three pairs of alternatives (eqs 4 and 5). We also explored the significance with $\alpha_{ij} = 0.0016$ as done for the NHST.

**Case Study for Passenger Vehicles.** A case study for a comparative LCA that evaluates the environmental performance of powertrain alternatives for passenger cars in Europe is used to illustrate the USMs. Comparative assertions are common among LCAs that test the environmental superiority of electric powertrains over conventional internal combustion engines. Several LCA studies have comparatively evaluated the environmental performance of hybrid, plug-in hybrid, full battery electric, and hydrogen fuel cell vehicles. Many of these studies describe multiple trade-offs between environmental impacts: while electric powertrains notably reduce tailpipe emissions from fuel combustion, various other impacts may increase (e.g., toxic emissions from metal mining related to electric batteries). Against this background, electric powertrains in passenger vehicles are an example of problem shifting and a sound case to test comparative methods in LCA.

**Goal and Scope.** The goal of this comparative LCA is to illustrate different USMs by applying these methods to the uncertainty analysis results for three powertrain alternatives for passenger cars in Europe: a full battery electric (FBE), a hydrogen fuel cell (HFC), and an internal combustion engine (ICE) passenger car. The functional unit for the three alternatives corresponds to a driving distance of 150 000 vehicle-kilometers (vkm). The scope includes production, operation, maintenance, and end of life. The flow diagram for the three alternatives can be found in the SI (Figure S.1, Appendix III). The cases have been
implemented in version 5.2 of the CMLCA software (www.cmlca.eu), and the same software has been used to propagate uncertainty. The five USMs have been implemented in a Microsoft Excel (2010) workbook available in the SI.

Life Cycle Inventory. The foreground system was built using existing physical inventory data for a common glider as well as the FBE and ICE powertrains as described by Hawkins and colleagues, whereas the HFC powertrain data is based on Bartolozzi and colleagues. The background system contains process data from ecoinvent v2.2, following the concordances described by the original sources of data. A complete physical inventory is presented in the SI (Appendix IV). The uncertainty of the background inventory data corresponds to the pedigree matrix scores assigned in the ecoinvent v2.2 database. In addition, overall dispersions and probability distributions of the foreground inventory data have been estimated by means of the protocol for horizontal averaging of unit process data by Henriksson et al. Thus, the parameters are weighted averages with the inherent uncertainty, spread, and unrepresentativeness quantified. Specifically, unrepresentativeness was characterized in terms of reliability, completeness, temporal, geographical, technological correlation, and sample size, to the extent possible based on the information provided in the original data sources. Further details of the implementation of parameter uncertainty are presented in the SI (Appendix IV).

Life Cycle Impact Assessment (LCIA). The environmental performance of the selected transport alternatives is assessed according to 10 midpoint impact categories, namely: climate change, eutrophication, photochemical oxidation, depletion of abiotic resources, acidification, terrestrial ecotoxicity, ionizing radiation, freshwater ecotoxicity, stratospheric ozone depletion, and human toxicity. The characterization factors correspond to the CML-IA factors without long-term effects (version 4.7), and exclude uncertainty. No normalization or weighting was performed, and the results are presented at the characterized level.

Uncertainty Calculations. Uncertainty parameters of background and foreground inventory data were propagated to the LCA results using 1000 MC iterations. We provide a convergence test for the results at the characterized level for all impacts and alternatives considered to show that this amount of MC runs is appropriate for this case study (SI, Appendix VI). Although other sources of uncertainty could be incorporated by means of various methods, we did not account for uncertainty due to methodological choices (such as allocation and impact assessment methods) or modeling uncertainties, neither due to data gaps that disallow the application of such methods. Also, correlations between input parameters was not accounted for. In our experimental setup, the same technology and environmental matrix was used to calculate the results for the three alternatives for each MC run. Thus, dependent sampling underlies the calculations of paired samples. This experimental setup is important because it accounts for common uncertainties between alternatives that are particularly important in the context of comparative LCAs. Although the five statistical methods under study could be applied to independent sampled data sets, it would lack meaning as common uncertainties would then be disregarded. Thus, only dependently sampled MC runs were explored for the purpose of the present research. These MC runs per impact are available in the Microsoft Excel (2010) workbook in the SI.

The five USMs are applied to the same 1000 MC runs dependently sampled for each of the three alternatives and for each impact. As all methods are pairwise, we apply them for three pairs of alternatives: ICE/HFC, ICE/FBE, and FBE/HFC.

RESULTS

Figure 1 shows the results for our comparative LCA following the classic visualization of deterministic characterization, in which results are directly superposed for comparison. All impacts considered are lower for the HFC except for depletion of abiotic resources. Both the ICE and FBE show various environmental trade-offs: the ICE performs worse than both the FBE and HFC in five impacts, while the FBE performs worse than the ICE and HFC in six impacts. Overall, the HFC performs better than both the FBE and ICE on most impacts considered. However, these results bear no information on their significance or likelihood, as no uncertainties are included.

The complete set of results for the ten impacts considered and the five methods are found in the Microsoft Excel (2010) workbook in the SI. The deterministic LCA results shown in Table 3, correspond to those in Figure 1: HFC shows a better environmental performance than both the ICE and FBE for all impacts except for depletion of abiotic resources. In addition, Table 3 shows the results for the five statistical methods and for three selected impacts that display discrepant results.

For the discernibility analysis, and taking acidification as an example, the ICE and FBE vehicles have higher acidification results than HFC in 100% of the runs (Table 3, white cells under discernibility). Thus, the ICE and FBE are likely to be discernible alternatives from the HFC for acidification. For photochemical oxidation and acidification, there are pairs of alternatives that are not likely to be discernible as the percentage of runs in which one alternative is higher than the other is close to 50% (see Table 3 darker blue cells).
The impact category relevance results show the highest relevance parameter for acidification for the pairs ICE/HFC and FBE/HFC (Table 3, dark red cells). Thus, for the comparison between ICE, FBE, and HFC vehicles, acidification is an impact that plays the most important role in the comparison. The lowest relevance parameter was obtained for the pair ICE/FBE for acidification as well as for the pair ICE/HFC for ionizing radiation these are impacts for which efforts to refine data would be most fruitful (Table 3, white cells under impact category relevance).

For the overlap area, the pair HFC/FBE has a large overlapping area for ionizing radiation and the pair FBE/ICE has a large overlap for acidification (Table 3, darker orange cells). Aspects contributing to the alternatives’ performance in ionizing radiation and acidification would be areas to prioritize in data refinement. Other pairs have almost no overlapping area for instance HFC/ICE for photochemical oxidation and HFC/FBE for acidification (Table 3, white cells under overlap area). This means, that the choice of an alternative between pairs, HFC/ICE and HFC/FBE, represents a greater effect on photochemical oxidation and acidification, respectively.

The results for the NHST consist of the \( p \)-values for the paired \( t \)-test performed and the decision to reject (yes) or to fail to reject (no) the null hypothesis. This latter outcome has been included in Table 3. The \( p \)-values for all impacts and pairs of alternatives are \(<0.0001\), and thus the null hypothesis was rejected in all cases (see worksheet “NHST” in the Microsoft Excel (2010) workbook in the SI). Therefore, results for all pairs of alternatives were significantly different for all impact categories (Table 3, purple cells). With the corrected significance level (\( \delta_0 \)) we re-evaluated the null hypothesis but still rejected the null hypothesis in all comparisons.

For the modified NHST the comparison between the ICE and FBE for the acidification impact, cannot reject (no) the modified null hypothesis. Yet in the case of the NHST method it is rejected. Table 3 does not correspond to a mirror matrix for this method because the direction of the comparison matters. For acidification, we see that the pair FBE/ICE is not significantly different as well as the pair ICE/FBE. Thus, in both comparisons the scores of the first alternative are not at least \( \delta_0 \) significantly higher than the scores of the second alternative. Therefore, the distance between the means of both alternatives is less than \( \delta_0 \) i.e., 0.2 standard error units. With the corrected significance level \( (\delta_0) \), we re-evaluated the null hypothesis but found no changes in the outcomes.

Cross Comparison of Methods. Exploring the results across methods for the same impact shows consistent results for most impacts, i.e., seven out of ten. A higher relevance parameter coincides with a smaller overlap area between distributions, and this generally coincides with well-discernible alternatives. Likewise, pairs of alternatives are more likely to have significantly different mean results when discernible. Below we focus our comparison of methods on three impacts (Table 3) that show discrepancies or conflicting results for some of the five methods.

For photochemical oxidation, the results for the five methods seem to agree to a large extent. Deterministic results show that HFC has the lowest characterized results among the three alternatives. However, according to the discernibility results, HFC is lower than FBE, for 83% of the runs. This shows that point-value results can be misleading, because there is a 17% likelihood that a point value would have given an opposite result. The overlap area results show a 0.63 overlap between the HFC and FBE on photochemical oxidation, indicating a mild difference (given the range of 0 to 1) in their performance. NHST and modified significance are in agreement with results from other methods and show significant different means for the two alternatives.

For acidification, results for some methods are consistent (Table 3). Discernibility of almost 100% along with a high relevance parameter and a low overlap area are shown for two pairs of alternatives HFC/ICE and HFC/FBE. Nonetheless, for the pair FBE/ICE discernibility results show a close call (FBE scoring only higher than ICE on acidification results for 45% of the runs) suggesting similar performances in acidification for FBE and ICE. This outcome is confirmed by the results of the impact category relevance (0.24), the overlap area (0.88), and the modified NHST where the null hypothesis is accepted and therefore no statistical difference can be established. NHST results, however, show a rejection of the null hypothesis that FBE and ICE have significantly different means for acidification, confirming that this pair of alternatives has significantly different acidification impacts—thus opposing the outcome of the other methods. As the sample size is large (namely 1000 observations), so is the

Table 3. Results for Selected Impacts (Those with Discrepant Outcomes between Some Methods) for the Comparative LCA of the Full Battery Electric (FBE) Vehicle, The Hydrogen Fuel Cell (HFC) Vehicle and the Internal Combustion Engine (ICE) Vehicle.*

| Impact            | Deterministic LCA (point values) | Discrimibility | Impact category relevance | Overlap area | NHST | Modified NHST |
|-------------------|----------------------------------|----------------|---------------------------|--------------|------|---------------|
| Photochemical     |                                  |                |                           |              |      |               |
| Oxidation         |                                  |                |                           | 0.24         | 0.68 |               |
|                   |                                  |                |                           |              |      |               |
|                    |                                  |                |                           |              |      |               |
| Acidification      |                                  |                |                           |              |      |               |
|                    |                                  |                |                           |              |      |               |
| Ionizing Radiation|                                  |                |                           |              |      |               |

*Tables display different results for the comparison of alternatives \( j \) and \( k \) for the reviewed uncertainty-statistics methods (USMs). The meaning of results per method is shown in the second row of the table together with the color labels.
Discernibility results show that ICE scores higher than HFC on parameter (0.34) with a high overlap area (0.79). However, the one hand, and the impact category relevance and overlap area results on the other hand. The HFC/ICE pair shows a low relevance so that the output falls within a spectrum, e.g., from 0 to 1 for overlap area, as opposed to a binary type output, e.g. fail to reject or reject the null hypothesis for NHST and modified NHST. Figure 2 shows the histogram for the distribution of HFC and ICE outcomes as well as the discernibility in a scattered plot, for better understanding the contradicting results between overlap area and discernibility. Here we can see that while the histograms overlap a considerable amount, the performance between the alternatives can still be considered statistically different since all the runs fall within one side of the diagonal in the scattered plot, which disregards the distance of each point to the diagonal.

**DISCUSSION**

We have reviewed, applied, and compared different methods for uncertainty-statistics in comparative LCA. We showed how deterministic LCA can lead to oversimplified results that lack information on significance and likelihood, and that these results do not constitute a robust basis for decision-making. In addition, we found that, while in most instances (seven out of ten impacts), the five methods concur with each other, we identified instances where the methods produce conflicting results. Discrepancies are due to differences in the setup of the analysis (i.e., overall or per run) which accounts or not for common uncertainties and due to accounting or not for the magnitude of the differences in performances. We identify two groups of methods according to the type of analysis they entail: exploratory and confirmatory methods. This division corresponds with the statistical theories by Tukey, in which data analysis initially requires an exploratory phase without probability theory, so without determining significance levels or confidence intervals, followed by a confirmatory phase determining the level of significance of the appearances identified in the exploratory phase. Exploratory statistics help delve into the results from uncertainty analysis and confirmatory methods evaluate hypotheses and identify environmental differences deemed statistically significant.

The NHST and modified NHST methods belong to the confirmatory group. Confirmatory methods are calculated per MC run, account for common uncertainties between alternatives and provide an absolute measure of statistical significance of the difference. These methods are appropriate for both single impact and multiple impact assessments and support statistical significance confirmation. NHST was shown to detect irrelevant differences of the means and to label them nevertheless as significant, while alternatives are considered to be indiscernible by modified NHST whenever the difference is small. The modified NHST approach is therefore recommended for confirmatory purposes and for all propagated LCA results, where the sample size in theory is indefinite and in practice is very large.

The impact category relevance and the overlap area methods belong to the exploratory group, as they help to identify some characteristics of uncertainty results among alternatives and impacts. These methods account for the magnitude of the
Figure 3. Decision tree to guide LCA practitioners on which uncertainty-statistics method (USM) to use for the interpretation of propagated LCA uncertainty outcomes in comparative LCAs. Thicker lines indicate recommended methods for confirmatory and exploratory purposes as per the considerations described in the main text. The type of information available from the uncertainty analysis results (in the following parentheses) determines the choice between impact category relevance (statistical parameters of the distributions) or overlap area (MC runs).

Difference per impact but do not consider common uncertainties or provide a measure of confidence or significance of the difference. These two methods are exclusively for exploring the uncertainty results in comparative LCAs with multiple impacts. Because the calculations are not per MC run, common uncertainties are disregarded and they do not serve confirmatory purposes. Disregarding common uncertainties can lead to instances where alternatives appear to be similar, while they actually perform different (like in ionizing radiation between ICE and HFC, Figure 2). Overcoming the fact that they do not account for common uncertainties would require generalization of the methods to “per run” calculations and could lead to a method similar to modified NHST accounting for the distance between means and common uncertainties.

Discernibility belongs to both groups. It accounts for common uncertainties, but it does not account for the magnitude of the difference per impact. It can be complimented with a p-value calculation, to develop its confirmatory potential, that would generate statistical significance based on the counts of the sign tests per pair. A proposal for such a procedure can be found in the SI (Appendix V) and involves the use of the binomial distribution. As it stands now, we consider it to serve an exploratory purpose similar to the impact category relevance or the overlap area, but with a different mechanism.

Both exploratory and confirmatory methods are valuable and synergistic in data-driven research, yet the specific choice of method is not straightforward for LCA practitioners given the discrepancies and characteristics previously discussed. Figure 3 provides guidance on which statistical methods LCA practitioners should use to interpret the results of a comparative LCA in light of its goal and scope, and when considering uncertainty. Figure 3 is in line with the main findings of this study. That is, exploratory methods facilitate the decision-making process by identifying differences and trade-offs in impacts between alternatives as well as by pointing to places where data refinement could benefit the assessment. Moreover, confirmatory methods effectively aid in making complex decisions from comparative assessments but should be used with statistical significance. For instance, carbon footprints, product environmental declarations, and LCAs aiming for comparative assertions disclosed to the public, should use confirmatory methods supporting conclusions with statistical significance calculations and accounting for common uncertainties.

Moreover, modified NHST appears to be the most well-developed method for confirmatory purposes. For exploratory purposes, however, we do not find a method that considers both core aspects: accounting for common uncertainties and for the extent of the differences per impact. Between these two aspects, common uncertainties are the most crucial aspect to address in a comparative context. Therefore, we recommend discernibility as the most suitable method for exploratory purposes while recognizing areas for improvement. Namely, we recommend that discernibility is further developed by adding a threshold of acceptable difference (as done in modified NHST) that, despite of being arbitrary, can better inform the exploration of trade-offs. We also recommend practitioners to exercise caution when applying overlap area and impact category relevance, and we recommend further developments of both methods to account for common uncertainties. Lastly, we call for caution when applying NHST regarding the sample size as it has been conceived for real samples and not for propagating uncertainty estimates where the sample size is in theory indefinite.

We encourage practitioners to use the excel workbook provided in the SI with the calculations made for the five methods in this paper which can aid them in delivering a more robust basis for decision-making.

As the use of statistical methods is becoming more frequent and increasingly important in environmental decision support, the definition of thresholds to determine the acceptable uncertainty demands attention. Arbitrarily set thresholds, such as p-value = 0.05, should be carefully used accounting for basic principles addressing misinterpretation and misuse of the p-value, as recently proposed by the American Statistical Association. In the field of LCA, we need practical guidelines to establish meaningful uncertainty thresholds for different applications. Methods like modified NHST and extended discernibility (see Appendix V), require such threshold levels to calculate statistical significance. We depart from the premise that various sources of uncertainties of the inputs have been adequately quantified and propagated to uncertainty results. The effects of the quality of uncertainty quantification and propagation on the interpretation of uncertainty results in comparative LCAs

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requires further study. Any outcome of any test is only as good as the quality of the input data, which for all studied methods corresponds to the results of an uncertainty analysis.

**ASSOCIATED CONTENT**

* Supporting Information
The Supporting Information is available free of charge on the ACS Publications website at DOI: 10.1021/acs.est.7b06365.

Additional calculations and case study details (PDF)
Implementation and results of five uncertainty-statistics methods (Microsoft Excel 2010) (XLSX)

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**REFERENCES**

(1) ISO. ISO 14044. Environmental Management—Life Cycle Assessment—Requirements and Guidelines; Switzerland, 2006.
(2) JRC-IES. ILCD Handbook. International Reference Life Cycle Data System. General Guide for Life Cycle Assessment; Ispra, Italy, 2010.
(3) Wei, W.; Larrey-Lassalle, P.; Faure, T.; Dumoulin, N.; Roux, P.; Mathias, J. D. Using the Reliability Theory for Assessing the Decision Confidence Probability for Comparative Life Cycle Assessments. Environ. Sci. Technol. 2016, 50 (5), 2272–2280.
(4) Ross, S.; Evans, D.; Webber, M. How LCA studies deal with uncertainty. Int. J. Life Cycle Assess. 2002, 7 (1), 47–52.
(5) Björklund, A. E. Survey of approaches to improve reliability in lca. Int. J. Life Cycle Assess. 2002, 7 (2), 64–72.
(6) Heijungs, R.; Lenzen, M. Error propagation methods for LCA—a comparison. Int. J. Life Cycle Assess. 2014, 19 (7), 1445–1461.
(7) Huibregts, M. A. J.; Giljum, W.; Ragas, A. M. J.; Reijnders, L. Evaluating uncertainty in environmental life-cycle assessment. A case study comparing two insulation options for a Dutch one-family dwelling. Environ. Sci. Technol. 2003, 37 (11), 2600–2608.
(8) Heijungs, P. J. G.; Guinée, J. B.; Heijungs, R.; de Koning, A.; Green, D. M. A protocol for horizontal averaging of unit process data—including estimates for uncertainty. Int. J. Life Cycle Assess. 2014, 19 (2), 429–436.
(9) Groen, E.; Heijungs, R.; Bokkers, E. A. M.; de Boer, I. J. M. Methods for uncertainty propagation in life cycle assessment. Environ. Model. Softw. 2014, 62, 316–325.
(10) Lloyd, S. M.; Ries, R. Characterizing, propagating, and analyzing uncertainty in life-cycle assessment. J. Ind. Ecol. 2007, 11 (1), 161–181.
(11) Heijungs, R.; Kleijn, R. Numerical approaches towards life cycle interpretation five examples. Int. J. Life Cycle Assess. 2001, 6 (3), 141–148.
(12) Gregory, J.; Noshardtavan, A.; Olivetti, E.; Kirchain, R. A Methodology for Robust Comparative Life Cycle Assessments Incorporating Uncertainty. Environ. Sci. Technol. 2016, 50 (12), 6397–6405.
(13) Prado-Lopez, V.; Seager, T. P.; Chester, M.; Laurin, L.; Bernardo, M.; Tylock, S. Stochastic multi-attribute analysis (SMAA) as an interpretation method for comparative life-cycle assessment (LCA). Int. J. Life Cycle Assess. 2014, 19 (2), 405–416.
(14) Prado-Lopez, V.; Wender, B. a; Seager, T. P.; Laurin, L.; Chester, M.; Arslan, E. Tradeoff Evaluation Improves A Photovoltaic Case Study. J. Ind. Ecol. 2016, 20 (4), 710–718.
(15) Henriksson, P. J. G.; Heijungs, R.; Dao, H. M.; Phan, L. T.; de Snoo, G. R.; Guinée, J. B. Product carbon footprints and their uncertainties in comparative decision contexts. PLoS One 2015, 10 (3), e0121221.
(16) Henriksson, P. J. G.; Rico, A.; Zhang, W.; Ahmad-Al-Nahid, S.; Newton, R.; Phan, L. T.; Zhang, Z.; Jiahiang, J.; Dao, H. M.; Phu, T. M.; Little, D. C.; Murray, F. J.; Satapornvaint, K.; Liu, L.; Liu, Q.; Haque, M. M.; Krujisfen, F.; De Snoo, G. R.; Heijungs, R.; Van Bodegom, P. M.; Guinée, J. B. Comparison of Asian Aquaculture Products by Use of Statistically Supported Life Cycle Assessment. Environ. Sci. Technol. 2015, 49 (24), 14176–14183.
(17) Heijungs, R.; Henriksson, P.; Guinée, J. Measures of Difference and Significance in the Era of Computer Simulations, Meta-Analysis, and Big Data.Entropy 2016, 18 (10), 361.
(18) Hertwich, E. G.; Hammitt, J. K. A decision-analytic framework for impact assessment part I: LCA and decision analysis. Int. J. Life Cycle Assess. 2001, 6 (1), 5–12.
(19) Grant, A.; Ries, R.; Thompson, C. Quantitative approaches in life cycle assessment—part 2—multivariate correlation and regression analysis. Int. J. Life Cycle Assess. 2016, 21 (6), 912–919.
(20) Groen, E. A.; Bokkers, E. A. M.; Heijungs, R.; de Boer, I. J. M. Methods for global sensitivity analysis in life cycle assessment. Int. J. Life Cycle Assess. 2017, 22 (7), 1125–1137.
(21) Kailath, T. The Divergence and Bhattacharyya Distance Measures in Signal Selection. IRE Trans. Commun. Syst. 1967, 15 (1), 52–60.
(22) Agresti, A.; Franklin, C. A. Statistics—The Art and Science of Learning from Data; Prentice Hall, Inc.: Upper Saddle River, 2007.
(23) Mittelhammer, R. C.; Judge, G. G.; Miller, D. J. Econometric Foundations; Cambridge University Press: Cambridge, 2000.
(24) Cohen, J. Statistical Power Analysis for the Behavioral Sciences, 2nd ed.; Associates, L. E.: Hillsdale, NJ, 1988.
(25) Hawkins, T. R.; Gausen, O. M.; Stromman, A. H. Environmental impacts of hybrid and electric vehicles—a review. Int. J. Life Cycle Assess. 2012, 17 (8), 997–1014.
(26) Samaras, C.; Meisterling, K. Life Cycle Assessment of Greenhouse Gas Emissions from Plug-in Hybrid Vehicles: Implications for Policy. Environ. Sci. Technol. 2008, 42 (9), 3170–3176.
(27) Nordelöf, A.; Messagie, M.; Tillman, A. M.; Ljunggren Söderman, M.; Van Mierlo, J. Environmental impacts of hybrid, plug-in hybrid, and battery electric vehicles—what can we learn from life cycle assessment? Int. J. Life Cycle Assess. 2014, 19 (11), 1866–1890.
(28) Notter, D. A.; Gauch, M.; Widmer, R.; Wager, P.; Stamp, A.; Zah, R.; Althaus, H. J. Contribution of Li-Ion Batteries to the Environmental Impact of Electric Vehicles (vol 44, pg 6550, 2010). Environ. Sci. Technol. 2010, 44 (19), 7744–7744.
(29) Majeau-Bettez, G.; Hawkins, T. R.; Stromman, A. H. Life Cycle Environmental Assessment of Li-ion and Nickel Metal Hydride Batteries for Plug-in Hybrid and Battery Electric Vehicles. Environ. Sci. Technol. 2011, 45 (10), 4548–4554.
(30) Granovskii, M.; Dinger (2); Rosen, M. A. Economic and environmental comparison of conventional, hybrid, electric and hydrogen fuel cells vehicles. J. Power Sources 2006, 159 (2), 1186–1193.
(31) Font Vivanco, D.; Freire-González, J.; Kemp, R.; Van Der Voet, E. The remarkable environmental rebound effect of electric cars: A macroeconomic approach. Environ. Sci. Technol. 2014, 48 (20), 12063–12072.
(32) Hawkins, T. R.; Singh, B.; Majeau-Bettez, G.; Stromman, A. H. Comparative Environmental Life Cycle Assessment of Conventional and Electric Vehicles. *J. Ind. Ecol.* 2013, 17 (1), 53−64.

(33) Bartolozzi, I.; Rizzi, F.; Frey, M. Comparison between hydrogen and electric vehicles by life cycle assessment: A case study in Tuscany, Italy. *Appl. Energy* 2013, 101, 103−111.

(34) Weidema, B.; Wesnaes, M. Data quality management for life cycle inventories—an example of using data quality indicators. *J. Cleaner Prod.* 1996, 4 (3), 167−174.

(35) Frischknecht, R.; Jungbluth, N.; Hans-jörg, A.; Gabor, D.; Dones, R.; Heck, T.; Hellweg, S.; Hischier, R.; Nemecek, T.; Rebitzer, G.; Spielmann, M. Overview and Methodology—Ecoinvent Report No. 1; Dübendorf, 2007.

(36) CML. *CML-IA Characterization Factors*; Leiden, 2016.

(37) Mendoza Beltran, A.; Heijungs, R.; Guinée, J.; Tukker, A. A pseudo-statistical approach to treat choice uncertainty: the example of partitioning allocation methods. *Int. J. Life Cycle Assess.* 2016, 21, 252−264.

(38) Andrianandraina; Ventura, A.; Senga Kiessé, T.; Cazacliu, B.; Idir, R.; van der Werf, H. M. G. Sensitivity Analysis of Environmental Process Modeling in a Life Cycle Context: A Case Study of Hemp Crop Production. *J. Ind. Ecol.* 2015, 19 (6), 978−993.

(39) Groen, E. A.; Heijungs, R. Ignoring correlation in uncertainty and sensitivity analysis in life cycle assessment: what is the risk? *Environ. Impact Assess. Rev.* 2017, 62, 98−109.

(40) de Koning, A.; Schowanek, D.; Dewaele, J.; Weisbrod, A.; Guinée, J. Uncertainties in a carbon footprint model for detergents: quantifying the confidence in a comparative result. *Int. J. Life Cycle Assess.* 2010, 15 (1), 79−89.

(41) Heijungs, R.; Henriksson, P. J. G.; Guinée, J. B. Pre-calculated LCI systems with uncertainties cannot be used in comparative LCA. *Int. J. Life Cycle Assess.* 2017, 22 (3), 461−461.

(42) Tukey, J. W. Exploratory data analysis as part of a larger whole. In *Proceedings of the 18th Conference on the Design of Experiments*; 1973; p 390.

(43) Tukey, J. W. We Need Both Exploratory and Confirmatory. *Am. Stat.* 1980, 34 (1), 23−25.

(44) Hellweg, S.; Mila i Canals, L. Emerging approaches, challenges and opportunities in life cycle assessment. *Science (Washington, DC, U. S.)* 2014, 344 (6188), 1109−1113.

(45) Wasserstein, R. L.; Lazar, N. A. The ASA’s Statement on p-Values: Context, Process, and Purpose. *Am. Stat.* 2016, 70 (2), 129−133.

(46) Mila I Canals, L.; Azapagic, A.; Doka, G.; Jefferies, D.; King, H.; Mutel, C.; Nemecek, T.; Roches, A.; Sim, S.; Stichnothe, H.; Thoma, G.; Williams, A. Approaches for addressing life cycle assessment data gaps for bio-based products. *J. Ind. Ecol.* 2011, 15 (5), 707−725.