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Authors
Motion, JP Michael
Huynh, Grace H
Szoka, Francis C
et al.

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Convection and Retro-Convection Enhanced Delivery: Some Theoretical Considerations Related to Drug Targeting

J. P. Michael Motion • Grace H. Huynh • Francis C. Szoka Jr. • Ronald A. Siegel

ABSTRACT Delivery of drugs and macromolecules into the brain is a challenging problem, due in part to the blood–brain barrier. In this article, we focus on the possibilities and limitations of two infusion techniques devised to bypass the blood–brain barrier: convection enhanced delivery (CED) and retro-convection enhanced delivery (R-CED). CED infuses fluid directly into the interstitial space of brain or tumor, whereas R-CED removes fluid from the interstitial space, which results in the transfer of drugs from the vascular compartment into the brain or tumor. Both techniques have shown promising results for the delivery of drugs into large volumes of tissue. Theoretical approaches of varying complexity have been developed to better understand and predict brain interstitial pressures and drug distribution for these techniques. These theoretical models of flow and diffusion can only be solved explicitly in simple geometries, and spherical symmetry is usually assumed for CED, while axial symmetry has been assumed for R-CED. This perspective summarizes features of these models and provides physical arguments and numerical simulations to support the notion that spherical symmetry is a reasonable approximation for modeling CED and R-CED. We also explore the potential of multi-catheter arrays for delivering and compartmentalizing drugs using CED and R-CED.

KEY WORDS blood brain barrier • convection enhanced delivery • finite element analysis • mathematical model • retro-convection enhanced delivery

ABBREVIATIONS CED convection enhanced delivery • ECF extracellular fluid • i.c. intracranial • ISF interstitial fluid • PDE partial differential equation • R-CED retro-convection enhanced delivery • s.c. subcutaneous

INTRODUCTION

Primary malignant brain tumors are a significant therapeutic challenge in spite of substantial advances in tumor imaging, neurosurgery, and radiation therapy. The efficacy of potent chemotherapy drugs is limited by biochemical and physiological barriers, including poor drug delivery to
the brain tumor mass and its peripheral regions (1–3), rapid clearance from the brain extracellular space (4), high intratumor pressure (5) and toxicity to normal brain tissue. More effective patterning of fluid movement through the tumor or diversion of fluid from entering normal brain parenchyma could improve brain tumor therapy.

Over the past decade, convection enhanced delivery (CED), employing a positive pressure infusion directly into the brain, has shown promising results in both animal models and clinical trials (6–9). CED distributes macromolecules, proteins, and particulate therapies into large volumes of tissue (10–12). Retro-convection enhanced delivery (R-CED), which removes interstitial fluid through a microdialysis catheter (13), has also been introduced to deliver drugs into brain tumors (14). Continuous flow of a hyperosmotic high molecular weight polymer solution, as the dialysate, drives fluid flow from the interstitial space into the catheter, lowering interstitial pressure and leading to convective flow of fluid, including drug, from capillaries into tissue. By themselves or in combination, CED and R-CED provide tools to pattern interstitial flow in the brain. Fig. 1 illustrates CED and R-CED.

Theoretical approaches of varying complexity, ranging from analytical to finite element models, have been developed to better understand and predict the interstitial distribution of material infused by CED (15–20). These models have also been used to predict features such as the interstitial fluid pressure, interstitial fluid velocity, tissue swelling, and transvascular fluid exchange rate during CED. Although these models do not recapitulate all aspects of fluid distribution in the brain following CED, they are instructive regarding what might be achieved in fluid patterning by a multi-catheter infusion protocol.

Recently, Wang and Olbricht published an analysis of R-CED driven by hydrostatic or osmotic flow across a tubular microdialysis membrane (21). It was shown that drug concentration near the catheter is enhanced when it cannot permeate through the membrane, but such enhancement is marginal when drug is permeable or semipermeable in the membrane. Removal of drug into the catheter largely defeats the purpose of R-CED, which is to draw drug into brain or tumor tissue from the capillaries.

Analytical models of flow and diffusion for both CED and R-CED can only be solved explicitly in simple geometries, and spherical symmetry is usually assumed for CED, while axial symmetry was assumed by Wang and Olbricht for R-CED (21). Although real systems are more complicated, in this article we provide physical arguments and supporting numerical studies indicating that spherical symmetry is a reasonable approximation in both CED and R-CED. We also explore the potential benefits of fluid delivery through multiple catheters. For example, drug-free fluid flow out of one catheter can be used to divert drug-containing fluid delivered from another catheter, offering protection to tissue surrounding the first catheter. Thus, drug delivered near the tumor/tissue interface might, in principle, be localized on the tumor side, with a nonspherical, nonsymmetric distribution. This idea is illustrated with a simple phantom construct.

**FLUID FLOW MODELING**

**Fluid Balance Equations**

Following previous analyses, we utilize a simplified modeling approach in which fluid flow through tissue is described by Darcy’s law,

\[ \tau = -K \nabla p \]  

(1)

![Fig. 1](https://example.com/fig1.png) Schematic illustration of fluid movement in the brain under the influence of CED or R-CED. **a** A CED catheter is implanted into the brain, and a solution is perfused under a positive pressure (black arrows). The therapeutic solution convects in response to the pressure field. This allows permeation and distribution of the therapeutic agent contained in the solution into the region of interest. **b** To remove fluid from the brain, a hyperosmotic solution is perfused into the brain using a microdialysis probe. The microdialysis membrane separates the hyperosmotic perfusate from the brain interstitial. Fluid then flows from the blood into the ISF and towards the microdialysis probe as diagrammed with the black arrows. The fluid then exits through the output tube of the probe.
and the equation for continuity of the fluid,
\[ -\varphi \nabla \cdot \vec{u} - \varphi L_{pc}(p - p_e) = 0 \] (2)

where \( p \) is interstitial hydraulic pressure at a given location, \( \vec{u} \) is local (vector) fluid velocity, \( p_e \) is effective or Starling pressure of the capillary bed calculated according to Starling’s law \( (p_e = p_i + \sigma(x - \pi_c)) \), where \( p_i \) and \( p_e \) and the intercapillary hydraulic and osmotic pressures, \( \sigma \) is the interstitial osmotic pressure, and \( s \) is the reflection coefficient of the capillary wall, \( \varphi \) is volume fraction of tissue available for interstitial flow, \( C_0 \) is hydraulic conductivity of interstitial space, \( k \) is hydraulic conductivity of interstitial space, \( L_{pc} \) is the filtration coefficient of the capillary walls.

The parameters \( p_e, \varphi, s, k, L_{pc} \) are all assumed to be constant for a given tissue (e.g. brain parenchyma, tumor). The velocity vector \( \vec{u} \) is taken as a volume averaged field variable, with volume averaging effects introduced at the level of the Darcy coefficient, \( K \). Combining Eqs. 1 and 2 obtains the equation for the difference between interstitial and effective, Starling capillary pressure, \( \bar{p} = p - p_e \)
\[ \nabla^2 \bar{p} = \kappa^2 \bar{p} \] (3)
where \( \kappa = \sqrt{L_{pc} s / K} \) has units of inverse distance.

Equation 3 is of the Helmholtz type. In the absence of fluid exchange between tissue and capillaries \( (L_{pc}=0) \) it reduces to Laplace’s equation, \( \nabla^2 \bar{p} = 0 \). More detailed treatments also consider drug transport by diffusion and exchange across capillary walls. Since our present interest is fluid flow, these contributions to drug transport will not be considered here.

CED and R-CED from a Spherically Symmetric Catheter Tip

To denote the flow of drug solution through an idealized spherically symmetric CED catheter tip of radius \( R_m \) and centered at the origin by \( Q \) using spherical coordinates to represent position, i.e. \( r = (x, y, z), |r| = \sqrt{x^2 + y^2 + z^2}, \), the velocity field around the source will be \( \vec{u} = u_r \hat{r}, r > R_m \). Equations 3 and 1 become, respectively,
\[ \frac{\partial^2 \bar{p}}{\partial r^2} + \frac{2}{r} \frac{\partial \bar{p}}{\partial r} = \kappa^2 \bar{p}, \quad r > R_m \] (4)

\[ u_r = -K \frac{\partial \bar{p}}{\partial r}, \quad r > R_m \] (5)

Fluid flow continuity at the tip/tissue interface prescribes the boundary condition
\[ Q = 4\pi R_m^2 \varphi \bar{u}_r(R_m) = -4\pi R_m^2 \phi K \frac{\partial \bar{p}}{\partial r} \bigg|_{r=R_m} \] (6)

Far from the tip, interstitial and capillary fluids are in Starling equilibrium, i.e.
\[ \bar{p}(r) \rightarrow 0, \quad r \rightarrow \infty \] (7)

The solution to Eqs. 4–7 is
\[ \bar{p} = \frac{Q}{4\pi \kappa K} e^{-\kappa(r-R_m)} \frac{1}{1 + \kappa R_m} \quad r > R_m \] (8)

\[ u_r = \left[ \frac{Q}{4\pi \varphi \kappa^2} \right] \left( \frac{1 + \kappa r}{1 + \kappa R_m} \right) e^{-\kappa(r-R_m)} \quad r > R_m \] (9)

The terms in the square brackets refer to pressure and flow that would occur in the absence of fluid exchange between tissue and capillaries, i.e. \( k=0 \), (Laplace equation solution). The remaining terms quantitate the relative effects of fluid exchange compared to interstitial flow. These terms rapidly decay to zero for \( r \gg 1/k \) and limit the region of influence of flow from the catheter. The quantity \( 1/k \) is recognized as a “screening length” over which flow across capillary walls buffers perturbations in pressure due to infusion.

When tip radius is significantly smaller than the screening length, i.e. \( \kappa R_m \ll 1 \), Eqs. 8 and 9 simplify to \( \bar{p} = q \kappa e^{-\kappa r}/4\pi \phi K (\kappa r) \) and \( u_r = \left[ q \kappa^2/4\pi \phi (\kappa r)^2 \right] (1 + \kappa r) e^{-\kappa r} \), respectively, for \( r > R_m \). In this case, pressure and velocity at a point beyond the tip surface decay according to the number of screening lengths the point lies away from the center of the tip.

To model R-CED, we must include the effects of the dialysis membrane, whose hydraulic permeability will be denoted by \( L_{pm} \). We retain spherical symmetry in the model. We assume, as will be argued below, that this simplification will not lead to great error. Taking the intercapillary Starling pressure as the reference, and assuming that the osmolyte (e.g. high MW dextran) cannot permeate through the dialysis membrane but all other solutes can, the relevant pressure inside the catheter lumen is \( \bar{p}_l = p_i - \pi_l - p_e \) where the subscript \( l \) refers to the lumen. For R-CED, this pressure will be negative. Flow continuity at the membrane/tissue interface warrants that
\[ L_{pm} [\bar{p}_l - \bar{p}(R_m)] = -\varphi K \frac{\partial \bar{p}}{\partial r} \bigg|_{r=R_m} \] (10)
Replacing Eq. 6 with Eq. 11, the pressure and velocity fields surrounding a spherical R-CED catheter become

$$\tilde{p} = (1 - \theta) \left( \frac{R_m}{r e^{\kappa(r-R_m)}} \right) e^{-\kappa(r-R_m)} \tilde{p}_1$$

$$= (1 - \theta) K \frac{R_m}{r^2} \left( \frac{1 + \kappa r}{1 + \kappa R_m} \right) e^{-\kappa(r-R_m)} \tilde{p}_1$$

$$r > R_m$$

where

$$\theta = \frac{1}{1 + L_{pa}R_m/\varphi e^{\kappa R_m}}$$

is the fraction of Starling pressure that is dissipated in the membrane. The cases $\theta = 0$ and $\theta = 1$ correspond, respectively, to membrane and tissue control of R-CED flow. For $\kappa R_m \ll 1$, Eq. 11 simplifies to $\tilde{p} = (1 - \theta)(R_m/r) e^{-\kappa r} \tilde{p}_1$.

**Nonspherical Catheter Tips**

Having presented equations for the idealized geometry, we turn to the importance of precise tip geometry. For CED, delivery is through the open end of a narrow shaft. For R-CED, tubular microdialysis membranes are used, and Wang and Olbricht’s work assumed cylindrical geometry. Calculations based on this assumption are strictly correct only for catheters with large axis-to-radius ratios or when looking at tissue that is very close to the catheter. We now argue that spherical symmetry often provides a useful and reasonably accurate approximation for CED and R-CED. This approximation is commonly used in the electrostatics of colloidal solutions, where the Helmholtz equation (linearized Poisson-Boltzmann equation) is prominent (22,23).

Let $d$ be the largest length scale of the catheter tip, such as its radius or half its length. Also let the radial coordinate, $r$, be a suitably chosen centroid of the catheter tip. Then our assertion is, roughly, that spherical symmetry will apply for $r > d$, and Eqs. 8, 9 and 11 will be good approximations. For $r < d$, shape effects are more important.

To further support this assertion, several cases were studied in the COMSOL 3.5a simulation environment (COMSOL, Inc., Burlington MA), which solves partial differential equations (PDEs), subject to appropriate boundary conditions, using the finite element method. This method, despite its approximations, is preferred over analytic solutions. Even for the simple case of two ideal spherical catheters delivering fluid at the same rate, superposition does not provide a correct solution since each catheter’s presence perturbs the flow pattern generated by the other catheter.

To solve PDEs in COMSOL, a finite domain corresponding to tissue is prescribed, as is the geometry of the catheter(s). The type of equation (usually Helmholtz in the present case) is then selected, and boundary conditions are prescribed at the catheter surfaces and at the edges of the domain. To minimize the effect of domain boundaries on the numerical solution, the domain should be large compared to catheter radius or length and distance between the catheter’s tip. In the present simulations, Dirichlet conditions (zero Starling pressure, similar to Eq. 7) are prescribed at the domain boundary. Neumann conditions (pertaining to pressure gradients) are prescribed at catheter boundaries. Since we are only interested in patterns, no attempt has been made to introduce physiological parameters, flows magnitudes, or specific Starling pressures.

As a first example, Fig. 2a shows that a cubic tip, with fluid flowing uniformly and equally out of each face, is surrounded by an essentially spherical pressure field, except very close to the surface. Placed side by side with a

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**Fig. 2** Finite element analysis of R-CED. a Finite element analysis of spherical and cubic “model” catheter tips. We designed objects with equal diameter and set boundary conditions such that the flux emitting from the cube and the sphere are the same, and $kr_m = 0.25$. Pressure variations are represented by color changes, and the arrows correspond to the direction of the velocity field with normalized magnitudes. b Finite element analysis of a CED catheter tip fed by unidirectional plug flow with $kr_m = 0.5$. c Finite element analysis of R-CED Flow with $kr_m = 0.5$ and $kd = 4$. The shaft tips are to be impermeable, and the surrounding edges were modeled as model membranes. Relative pressures are mostly negative close to the membrane where reverse flow is being generated.
spherical tip with the two tips separated by a sufficient
distance that their interaction is small, and with equal flow
emerging from the two tips, the two objects produce
essentially identical pressure and flow fields away from
their surfaces, while fields near the surfaces depend on
shape. Fig. 2b shows simulations of delivery from a shaft,
with unidirectional flow to the lumen, which opens at its
end into the tissue. The outer body of the shaft is
impermeable to fluid flow. For simplicity, flow inside the
shaft is modeled as plug instead of Poisseuille flow. This
impermeable to fluid flow. Intuitively, as one moves farther away
from the tip, the surface area of the isobar becomes larger
compared to the cross-sectional area of the shaft. The shaft
therefore becomes much less important in “shaping” the
front. Fig. 2c displays the flow pattern into a cylinder,
representing R-CED into a microdialysis membrane. The
axial/radial ratio is 8. Close to the membrane, the
(negative) pressure contours are nearly cylindrical, but they
round out as one moves away from the tube. With a smaller
value of $k$ (larger 1/$k$), more such contours would be
discernable.

Multiple Catheter Delivery

The previous sections show that catheter shape has little
effect on pressure and flow profiles once fluid moves a
sufficient distance from the catheter tip. We now consider
the effects of flow from one catheter on flow from a second
catheter. The simplest situation is two identical catheters
placed at a distance from each other in a medium (tissue)
with uniform properties. Such a system is physically
modeled (see below) using an agarose gel phantom.
Suppose that one catheter delivers drug, while the other
delivers a drug-free, blank solution. If flows from the two
catheters are equal, then the flows will collide at the
“mirror” plane perpendicular to the two catheters and
proceed along that plane. This phenomenon is illustrated
by the flow arrows in Fig. 2a. Now suppose that flow from
the “blank” catheter is stronger. Then, the fluids will collide
along a surface that is closer to and bent around the drug-
delivering catheter. If the former and latter catheters are
properly placed inside and outside of the tumor, and flows
are properly selected, based on the tissue properties of
tumor and brain parenchyma (including differences in
tissue permeability, capillary densities and filtration coef-
ficients, and the absence of lymphatics in tumor, factors
which give rise to increased interstitial pressure in tumor), it
seems possible to focus drug delivery into the tumor and
substantially reduce exposure in the parenchyma. Conversely,
flow of a radioprotective agent from outside the tumor could
be “steered away” from tumor tissue by flow of blank solution
from a catheter inside the tumor.

A second possible dual probe configuration would
involve convective drug delivery from one catheter and
fluid removal by the other. Note that the latter catheter is
not used in the same way as has been previously considered
for R-CED, since drug is not being pulled out of the
circulation through capillaries, but rather is supplied by the
delivery catheter. In this case, flow is predicted from the
delivery catheter to the removal catheter, with a pattern
resembling the alignment of iron filings over two-pole
magnet. For reasons already identified by Wang and
Olbricht, this technique seems less promising than dual
CED, since it is more difficult to pull osmotically than it is
to push hydraulically, due to added hydraulic resistance
from the microdialysis membrane and tradeoffs between
osmotic pressure and viscosity of the dialysate (14), and
since drug will be lost into the removal catheter, unless that
catheter’s membrane is impermeable to drug.

DUAL PROBE CED IN AN AGAROSE GEL
PHANTOM

Dual probe CED experiments were carried out in an
agarose gel phantom by adapting methods that have been
described elsewhere for acute stereotactic infusion
(10,24,25). Bankiewicz and colleagues (26) have used a
similar system to visualize fluid distribution following single
probe CED. Briefly, cannulae were prepared from fused
silica tubing with an outer diameter of 0.16 mm (Polymicro
Technologies, Phoenix, AZ), extending 1–2 mm from the
tip of a 24 gauge needle used for support (26). Cannulae
were inserted into the 0.5% agarose gel (UltraPure
Agarose, 15510-019, Invitrogen, Carlsbad, CA), prepared
immediately before use, approximately 8 mm below the
surface of the gel, with tip outlets separated by 2 mm. An
external syringe pump (Bioanalytical Systems Inc., West
LaFayette, IN) was used to infuse solutions containing dyes
(67 kD albumin-Alexa Fluor 647 in one cannula and 3 kD
Texas Red-dextran in the other) at an increasing flow rate
as follow 0.1 mL/min for 5 min, 0.2 mL/min for 5 min,
0.5 mL/min for 5 min, and 0.8 mL/min for 30 min for a
total volume of 28 mL infused. Following the infusion, the
probes were removed slowly over 1 min. Photographs were
taken by slicing the agarose phantom and imaging on a
Kodak Imagentation 4000. Alexa Fluor 647 was visualized
individually using the 625 nm excitation filter and the
700 nm emission filter. Texas Red was visualized individ-
ually using the 535 nm excitation filter and the 600 nm
emission filter.

Fig. 3a shows the optical image of the two probes, with
Alexa Fluor in blue and Texas Red in red. Fluorescence

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images of individual probes are shown in Fig. 3b and c. While a small amount of each probe may have flowed upward around the cannulae, most flow was into the gel, and the two dyes are located in nearly hemispheric regions, indicating substantial nonoverlap of the flows. Close inspection reveals, however, that the Texas Red moves a little farther, and it “invades” the region that is predominantly Alexa Fluor. These observations are most likely due to diffusion, which will be greater for Texas Red because of its lower molecular weight.

CONCLUDING REMARKS

This paper has focused on the convective aspects of CED and R-CED in the brain. We have argued that, for many situations, both of these modalities can be modeled reasonably well using simple spherically symmetric solutions to the Helmholtz equation, which accounts for pressure and flow fields around single catheters. While real catheters may have different shapes, spherical fronts develop away from the catheter. Because the volume of the spherical shells increases as one moves away from the central source, the pressure and flow fields for most of the affected tissue are relatively insensitive to catheter shape, provided boundary conditions such as total flow are properly set. Real-time imaging of CED infusions into primate brains demonstrates that tip dimensions and flow rates of currently used catheters in CED protocols generate initial drug distribution with spherical symmetry in homogeneous brain regions (27).

However, spherical symmetry is lost when the infused volume reaches regions of the brain with different tissue properties, leading to channeling effects and uneven drug profiles. As a result, we must keep in mind that although spherical symmetry is a valid approximation within homogenous tissue regions, anatomical differences in the brain can alter expected drug profiles and concentrations. The model for filtration across capillary walls is based on the classical Starling hypothesis, with hydrostatic and osmotic pressures inside the tissue assumed to be volume-averaged field variables. A more recent interpretation of transcapsillary wall filtration suggests a more complex picture, however, with concentration polarization of osmolytes adjacent to the endothelial glycocalyx affecting osmotic flow (28). These effects may alter the precise pressure and flow distributions in tissue, but they are unlikely to alter the qualitative behavior.

Although convection through tissue and filtration of fluid across capillaries have been the main emphasis of this paper, transport of drug by diffusion and by solvent drag across capillary walls should be incorporated into more complete descriptions (19–21). As suggested by the phantom experiment, diffusion plays a noticeable but secondary role in distribution of drug. Its effect is expected to be most pronounced in regions where fluid flow is slow (low Peclet number), i.e. away from the catheter, provided drug has not been degraded or removed before reaching those regions.

We have also demonstrated the effect of dual catheters in shaping flow fields and argued that by this means one might steer chemotherapy out of regions of the brain where toxic side effects could occur. Of course, one might consider the effects of multiple catheters in generating drug delivery patterns, subject to surgical constraints. Diffusion may blur the boundaries between flow fields derived from neighboring catheters, however, as illustrated in Fig. 3.

In addition to drug localization, drug patterning by multiple catheters could be useful when drug should be distributed through an entire brain region while sparing critical tissues. This could be accomplished by infusing a nontoxic saline solution into the critical area while simultaneously infusing the drug into the larger regional space.

In order to enable such combination therapies, it will be necessary to know the tissue properties in advance of pattern planning or to use real-time imaging (9,27,29) such that the infusion flow rates could be altered based on the distribution of the ongoing infusion.

We conclude by suggesting further strategies which use CED and R-CED. In one example, a rapidly eliminated blood-brain-barrier-permeable drug could be administered systemically, and a saline solution could be infused into the tumor. The pressure of the saline infusion would reduce drug extravasation into the tumor but would have no such effect in normal tissue. Potential applications include the infusion of radio- or cryoprotectants (30), whereby protectant would accumulate in normal tissue, but tumor would remain susceptible to radiation or cryo therapies.

Parameters governing transport in the brain may be susceptible to manipulation, allowing for alteration in drug...
distribution. For example, interstitial hydraulic conductivity might be altered using enzymes such as hyaluronidase to degrade the extracellular matrix (31). Capillary permeability, on the other hand, might be altered by angiogenesis regulators such as VEGF. Such alterations, in addition to changing the region of influence of a catheter, might alter the pressure requirements on catheters to establish a desired drug distribution.

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