Frequency-Dependent Selection Predicts Patterns of Radiations and Biodiversity

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Abstract

Most empirical studies support a decline in speciation rates through time, although evidence for constant speciation rates also exists. Declining rates have been explained by invoking pre-existing niches, whereas constant rates have been attributed to non-adaptive processes such as sexual selection and mutation. Trends in speciation rate and the processes underlying it remain unclear, representing a critical information gap in understanding patterns of global diversity. Here we show that the temporal trend in the speciation rate can also be explained by frequency-dependent selection. We construct a frequency-dependent and DNA sequence-based model of speciation. We compare our model to empirical diversity patterns observed for cichlid fish and Darwin’s finches, two classic systems for which speciation rates and richness data exist. Negative frequency-dependent selection predicts well both the declining speciation rate found in cichlid fish and explains their species richness. For groups like the Darwin’s finches, in which speciation rates are constant and diversity is lower, speciation rate is better explained by a model without frequency-dependent selection. Our analysis shows that differences in diversity may be driven by incipient species abundance with frequency-dependent selection. Our results demonstrate that genetic-distance-based speciation and frequency-dependent selection are sufficient to explain the high diversity observed in natural systems and, importantly, predict decay through time in speciation rate in the absence of pre-existing niches.

Introduction

Speciation is one of the most complex phenomena in nature, yet the effects of its tempo and mode for biodiversity patterns are still controversial [1,2]. Pre-existing niches is considered the dominant mechanism explaining the initial explosion of diversity observed in radiations [3–7]. In contrast, non-adaptive radiations [8,9] driven by niche-independent mechanisms such as sexual selection, rapid range expansion across multiple barriers or the simultaneous formation of multiple geographical barriers, dispersal limitation or isolation by distance without physical barriers due to genetic incompatibilities do not predict such a temporal trend of declining speciation rates during a radiation [10–13]. Although ecological opportunity (the availability of an unoccupied adaptive zone) or rapid range expansion across multiple barriers can explain rates of diversification in some radiating lineages, this is not sufficient for a radiation to occur [14–17]. Instead of attributing the propensity to have a radiation with decaying through time speciation rates to external influences like niche availability or rapid range expansion an alternative hypothesis can be based in the genome properties evolved during the evolutionary history of organisms. We explore this hypothesis using two models, one with frequency-dependent selection and one without it. Both models involve DNA sequence-based evolution of populations via a process of sexual reproduction, assortative mating, mutation, and genetic-distance-based speciation.

The models we have analyzed in the present study are similar in spirit to previous speciation models [12,13,18,19] but different in two key details: (1) no approximations of the tempo and mode of speciation incorporating sexual reproduction and frequency-dependent selection have previously been shown to explain observed patterns of decay through time of the speciation rate during a radiation without invoking pre-existing niches. Furthermore, we show that the decay through time of the speciation rate during a radiation without invoking pre-existing niches has dramatic consequences to species richness and diversity, and (2) we contrast the models with two small radiations for a broad range of parameter values: the Tilapia cichlid genus [11] and the Darwin’s finches [20], two groups where assortative mating has been previously documented [21–24]. We note that larger radiations cannot be handled computationally. This represents a
Author Summary

Ecological opportunity, or filling a pre-existing unoccupied adaptive zone, is considered the dominant mechanism explaining the initial explosion of diversity. Although this type of niche filling can explain rates of diversification in some lineages, it is not sufficient for a radiation to occur. Instead of attributing the propensity to have an explosion of new species to external influences like niche availability, an alternative hypothesis can be based in frequency-dependent selection driven by the ecology in which organisms are embedded or endogenous sources mediated by gametes during fertilization. We show that genome diversification driven by higher reproductive probability of rare genotypes generates rapid initial speciation followed by a plateau with very low speciation rates, as shown by most empirical data. The absence of advantage of rare genotypes generates speciation events at constant rates. We predict decline over time and constant speciation rate in the cichlids and Darwin’s finches, respectively, thus providing an alternative hypothesis for the origin of radiations and biodiversity in the absence of pre-existing niche filling. In addition to predicting observed temporal trends in diversification, our analysis also highlights new mechanistic models of evolutionary biodiversity dynamics that may become suitable to generate neutral models for testing observed patterns in speciation rates and species diversity.

current limitation to explore broad patterns of speciation and diversity that requires further research.

We simulated the evolution of a population whose members, at the beginning, have identical genomes. The population evolves under the combined influences of sexual reproduction and mutation (Text S1). During reproduction, potential mates are identified from those whose genomes are sufficiently similar to that of the reproducing individual ($q_{\text{not}}$). This parameter implicitly captures the effects of the accumulation of genetic incompatibilities by prezygotic or postzygotic reproductive isolation [18,25–27]. A mate is chosen from this set at random. An offspring is then dispersed in the environment. This minimal form of mating called assortative mating [13,28,29] is sufficient for speciation at least when there is no genetic linkage [18,19]. Genomic similarity between two individuals is defined as the proportion of identical nucleotides along the genome. The genomic similarity among individuals can be represented by an evolutionary graph in which nodes are individuals and edges connect reproductively compatible individuals [30] (Figs. 1 and 2). We identify a species as a group of organisms reproductively separated from all the others by genetic restriction on mating, but connected among themselves by the same condition. Thus, two individuals connected at least by one pathway through the evolutionary graph are considered conspecific, even if the two individuals themselves are reproductively incompatible.

We consider three main assumptions that allow us to approximate the tempo of speciation and also to identify the conditions for each of two alternative modes of speciation in the evolutionary graph: (1) Our density of individuals is one per site, and these numbers are kept constant by assuming zero-sum dynamics. Birth-death zero-sum stochastic models are equivalent to their non zero-sum counterparts at stationarity [31]; (2) Factors influencing speciation may differ between regions of the genome, and regions of the genome involved in reproductive isolation may differ between taxa and the temporal stages of the speciation process [32]. In our model, the genome of each individual is considered effectively infinite (i.e., a very large string of nucleotides, Text S1), and (3) The mate choice function explaining the viability of the offspring is given by a step-shaped function. This is the simplest representation of Dobzhansky-Muller reproductive incompatibility [33–35]. Functions with equal viability in a range $[q_{\text{min}}, q_{\text{max}}]$ (see Material and Methods), declining linearly and exponentially [12] give qualitatively the same results as the results presented here using the step-shaped function.

At the beginning of the simulation, all individuals are reproductively compatible, corresponding to a completely connected graph. Because of mutations that can eventually reduce genetic similarity below the threshold required for mating, the graph will lose connections as generations pass (Fig. 1). The rate at which connections are lost in the evolutionary graph, and thus the tempo of speciation, depends on the mechanisms driving genome diversification.

Figure 1. Model of evolution. In each time step, first an individual dies. Second, parents are selected for reproduction (dotted square). Third, the dead individual is replaced by an offspring. Lastly, we recompute the species number and abundance. We then repeat the cycle. In this case the graph has two species with 5 (red circles) and 4 (blue circles) individuals.
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To explore the tempo of speciation and its implications for biodiversity patterns, we generated a second model with negative frequency-dependent selection. In this model there are no external factors creating pre-existing niches, which can be populated only by individuals of a specific genotype and can be filled up to a carrying capacity. In contrast, any rare genotype has higher fitness than common types. The reason may be natural selection driven by the ecology in which the organism is embedded (e.g., bacteria or pathogens attacking reproductive proteins of common types without altering the probability to die among individuals) [36,37] or some form of sexual selection that lead to rare-type advantage (e.g., sexual conflict, molecular incompatibility or heterozygote advantage in sexually selected genes) [38–40] and have more success at mating, whereas common types are likely–but not guaranteed–to become rare. Despite potential costs of the rare types (i.e., Allee effects, mating costs, etc), experimental and theoretical studies have shown that the selective value of a given genotype is often a function of its frequency in the population [41–46]. In summary, frequency-dependent selection in this context is a type of sexual selection with niches not imposed from outside the system but created by rare types with greater mating success that can spread their alleles more quickly through the population. Apart from the asymmetry introduced by the different reproductive probabilities at the individual level, these two models are identical (Text S1).

Results

With appropriate parameter values satisfying the mathematical condition required for speciation ($q^\min > Q^*$ where $Q^*$ is the genetic similarity matrix at equilibrium) both models can produce speciation events (i.e., sexual isolation of subpopulations in the genome space, Equation A-30 and Box 1 in Text S1).

We identified two distinct modes of speciation that can, under the right conditions, occur in the evolving graph: mutation-induced speciation and fission (Fig. 1). Mutation-induced speciation happens when a newly produced offspring is disconnected from its parents. This form of speciation requires the mutation rate to exceed some minimum value ($\mu^\min$) necessary to satisfy the inequality $q^k < q^\min$, where $k$ is the offspring and $j$ are the parents of $k$ (Fig. 2). Because the minimum number of steps equals 1, the minimum mutation rate to have mutation-induced speciation is given by:

$$\mu^\min = \frac{-\log\left(\frac{2q^\min}{1+q^\min}\right)}{2}. \quad (1)$$

For example, if offspring become inviable once genetic divergence exceeds 5% (i.e., $q^\min = 0.95$), then the minimum mutation rate needed to achieve mutation-induced speciation is $\approx 1.3 \times 10^{-2}$. There is a second mode of speciation which is also a consequence of mutations in the evolutionary graph. We call this mode “fission” because it takes place when the death of an individual breaks a link in what was the sole genetic pathway connecting some members of a species; this gives rise to one or more new species. Because of the strict condition for mutation-induced speciation to happen, fission is the only mode of speciation in the biologically relevant portion of model parameter space (Section A3 in Text S1).

The speciation rate ($v$) in the genetic similarity matrix ($Q$) has two different dynamics according to the initial minimum genetic similarity value to have fertile offspring ($q^\min$):

$$v = \begin{cases} 0 : Q^* > q^\min \rightarrow Q^* &= \frac{1}{\theta+1} \\ \frac{-2\mu + \log\left(q^\min + 3/4\right)}{\log(q^\min)} : Q^* < q^\min, \end{cases} \quad (2)$$

where $Q^*$ is the expected mean genetic similarity in the matrix $Q$ at equilibrium [18], $\theta = 4J\mu$ with $J$ the population size. If $Q^* < q^\min$, then $v$ is the rate of dropping links in the evolutionary
Discussion

Most speciation studies have concluded that sympatric speciation only occurs if a stringent set of conditions is met \([4,7]\). Likewise, for the models we have explored, sympatric speciation can be highly unlikely or even impossible in biologically relevant areas of parameter space (i.e., \(q_{\min} < Q' = \frac{1}{\theta+1}\) where \(\theta = 4J\mu\), Text S1). Note, however, that even though geographical barriers and dispersal limitation, and/or range expansion have played an important role in radiations, these factors do not generate decay through time in speciation rate in the absence of niche filling \([10–13]\) (see also Fig. 5 in Text S1). Interestingly, the absence of frequency-dependent selection does not capture the exponential growth in number of species in the last stage of the Darwin’s finches radiation. Time lag for extinctions \([50]\), taxonomic splitting but also the increase in heterogeneity with time in the Galápagos archipelago (i.e., more islands, habitat diversity and food types) \([20]\) are some of the factors that may hamper model predictions in this case. Nevertheless, the balance of results for both the cichlids and the Darwin’s finches suggest that neutral and frequency-dependent selection mechanisms have played a role in radiating lineages.

Current biodiversity theory, from population genetics \([13]\) to island biogeography and its extensions \([54]\), explain species abundance patterns for many groups, but cannot predict different trends in the tempo of speciation nor their implications for radiations and diversity patterns. The models we have explored generate alternative tempo of speciation and these models can be compared with the patterns of diversity underlying classic radiations. In the context of these models, we have also determined the conditions necessary for the mutation-induced mode of speciation; if these are not met, then fission must be the only speciation mode. Finally, we have shown that frequency-dependent selection generates more symmetric and larger incipient species abundances, resulting in lower extinction rates. These results reinforce the notion that the incipient species abundance can have a dramatic impact on contemporary diversity patterns \([54]\), and suggest that both the tempo and mode of speciation themselves have a large effect on current community dynamics.

Alternative models of speciation that incorporate additional molecular or ecological components exist (i.e., spatial heterogeneity and dispersal limitation \([19,55]\), recombination rate, insertions and deletions \([56]\) and the explicit mechanisms that cause genetic incompatibilities \([57,58]\)); however, it is not yet possible to evaluate these models with speciation rates and diversity data.

In summary, the particular mechanisms underlying the dynamics of the evolutionary graph affect the tempo of speciation and diversity, but we nevertheless find theoretical distributions in agreement with the observed patterns of radiations and biodiversity for diverse taxa. Underlying the result are two simple models of a sexually reproducing population with and without frequency-dependent selection and with mating restrictions that depend on genetic distance. By examining these models under different parameter combinations and confronting them with data, we conclude that the properties of genomes during lineage diversification may influence patterns of radiations and biodiversity and the pre-existing environmental niches are not necessary for radiations to occur.

Materials and Methods

Our simulation is a stochastic, individual-based, zero-sum birth and death model of a sexual population with overlapping generations and age-independent birth and death rates. For the simulations reported in the paper, we considered \(J\) haploid and hermaphroditic individuals where only one individual can exist in each site. Genomes consist of an infinite string of nucleotides and the genomic similarity between two individuals is defined as the proportion of identical nucleotides along the genome. Reproduction starts with a randomly selected individual looking for a mate...
among all the sufficiently similar individuals. To qualify, an individual must have a genetic similarity greater than the minimum value required for fertile offspring. From all such potential mates, we select the second parent at random. In the frequency-dependent selection model, individuals with few connections, and therefore with more rare alleles, have more
success at mating and their alleles spread quickly through the population.

Mating produces a haploid offspring that differs from both parents following free recombination and mutation (Text S1). Each nucleotide is inherited from one of the parents with the same probability. The results reported here are for asynchronous mating. Synchronous mating gave similar results, although speciation times were typically longer. According to tests of...
multiple model variants in the model without frequency-dependent selection, including parameter variation, self-incompatibility (i.e., by adding a $q^{\text{max}}$ to limit the reproduction of excessively similar individuals, Fig. 5a in Text S1), and mating and dispersal limited to adjacent patches (i.e., 8-patch Moore neighborhood) with a grid without a wrapped torus (Fig. 5b in Text S1). Our results apply quite generally, with the key required properties to generate declining through time speciation rates being the limitations on genetic distance associated with mating and the frequency-dependent selection mechanism.

Results for Fig. 3 are obtained by time-averaging over 10 replicates lasting $2 \times 10^3$ generations each. Given $J$ individuals in the initial population, a generation is an update of $J$ time steps. Parameter variation does not affect the overall behavior.

Results for Fig. 4 are obtained after $10^2$ replicates for each parameter combination lasting $2 \times 10^3$ generations each. We sampled the transients (each generation) and the steady state at the end of each replicate for the species through time and species abundance. We have explored $9 \times 10^3$ parameter combinations in the range $\mu \in [10^{-2},10^{-4}]$, $q^{\text{min}} \in [0.75,0.98]$, and community size, $J = [10^2,2 \times 10^3]$ that satisfy the mathematical condition required for speciation ($q^{\text{min}} > Q$, equation A-30 and Box 1 in Text S1). Our results apply quite generally in a broad range of community size (Fig. 3 in Text S1) and speciation rates (Fig. 4 in Text S1).

The fit to the number of species and speciation events through time was done following these steps: 1) Normalize time for observed data and each simulation from the first speciation event to present time within the range $[0,1]$, 2) From each possible interval, starting with the size of the data until the size of the output in each simulation ($2 \times 10^3$ generations with increments of 1 generation at each time), we generated the sequence of speciation times that minimizes the difference with the observed speciation times, and 3) Identify the best fit as the one that minimizes the sum of the absolute values of the misfits:

$$M((x_0^{(1)}, y_0^{(1)})\ldots(x_0^{(S)}, y_0^{(S)})(\theta, q^{\text{min}}) = \sum_{i=1}^{S} m_i$$

where $m_i$ is defined as $(|x_0^{(i)} - x_{\text{sim}}^{(i)}| + |y_0^{(i)} - y_{\text{sim}}^{(i)}|)$, i.e., in terms of the misfit between observed and simulated species richness, $|x_0^{(i)} - x_{\text{sim}}^{(i)}|$, and the misfit in the timing of speciation events $|y_0^{(i)} - y_{\text{sim}}^{(i)}|$. $\theta = 4J\mu$ and $q^{\text{min}}$ are our model parameters. Our search is performed for a broad range of plausible empirical values for $J\mu$ and $q^{\text{min}}$ constant and satisfying $q^{\text{min}} > Q$ (Text S1).

If our errors per data point are a random variable $M$, following the exponential distribution, $M \sim \exp(-m_i)$, and, assuming error independence, our measure of misfit $M$ is the model negative log-likelihood [59]. Confidence intervals have been calculated by taking the percentiles 0.05 and 0.95 from the distributions of values of different model replicates. Model replicates were generated with the best parameter estimates for $\theta$ and $q^{\text{min}}$ along with a family of pairs within 2 log-likelihood units away from the minimum [60] (Fig. 4 in Text S1).

Supporting Information

Text S1 Frequency-dependent selection predicts patterns of radiations and biodiversity. Found at: doi:10.1371/journal.pcbi.1000892.s001 (0.22 MB PDF)

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Author Contributions

Conceived and designed the experiments: DPV. Analyzed the data: CJM SA. Contributed reagents/materials/analysis tools: CJM DA JR SA. Wrote the paper: CJM DA DPV JR SA.

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