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Wideband trapping of light by edge states in honeycomb photonic crystals

Chunfang Ouyang\textsuperscript{1}, Dezhuan Han\textsuperscript{1}, Fangyuan Zhao\textsuperscript{2}, Xinhua Hu\textsuperscript{2}, Xiaohan Liu\textsuperscript{1} and Jian Zi\textsuperscript{1}

\textsuperscript{1}Department of Physics, Key Laboratory of Micro- and Nano-Photonic Structures (Ministry of Education), and Key Laboratory of Surface Physics, Fudan University, Shanghai 200433, People’s Republic of China

\textsuperscript{2}Department of Materials Science and Laboratory of Advanced Materials, Fudan University, Shanghai 200433, People’s Republic of China

E-mail: huxh@fudan.edu.cn and jzi@fudan.edu.cn

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Abstract

We study theoretically light propagations at the zigzag edge of a honeycomb photonic crystal consisting of dielectric rods in air, analogous to graphene. Within the photonic band gap of the honeycomb photonic crystal, a unimodal edge state may exist with a sharp confinement of optical fields. Its dispersion can be tuned simply by adjusting the radius of the edge rods. For the edge rods with a graded variation in radius along the edge direction, we show numerically that light beams of different frequencies can be trapped sharply in different spatial locations, yielding wideband trapping of light.

Some figures may appear in colour only in the online journal

Graphene, a flat monolayer of graphite with carbon atoms arranged in a honeycomb lattice, has many interesting physical properties with great promise in nanoelectronics owing to its unique electronic properties, e.g., conical dispersion (Dirac cones) in the electronic band structure \cite{1}. With inspiration from graphene, its photonic analog, namely, two-dimensional photonic crystals \cite{2-4} that possess Dirac cones in photonic band structures, have drawn considerable attention in recent years \cite{5-12}. The existence of Dirac cones may lead to many interesting optical phenomena such as conical diffraction and gap solitons \cite{5}, pseudodiffusive transport of light \cite{6, 11}, zitterbewegung of photons \cite{8} and the realization of zero-refractive-index materials \cite{12}.

Wideband trapping of light, also called ‘rainbow’ trapping, is an optical phenomenon where light of different frequencies can be slowed down and stopped at different spatial positions in specially designed waveguides \cite{13}. It has many potential applications ranging from optical information storage to enhanced light–matter interactions \cite{14}. Several structures for realizing wideband trapping have been proposed, including metamaterial waveguides \cite{13, 15}, plasmonic waveguides \cite{16}, metal-coated optical nanowaveguides \cite{17} and plasmonic gratings \cite{18, 19}. However, these structures may inevitably suffer from a serious problem of optical loss due to the constituting metals, which are rather lossy especially in the visible regime. In contrast, dielectric photonic crystal waveguides can also slow light with a very small loss \cite{20, 21}, which could be exploited in light trapping \cite{22}. But they are usually multimodal \cite{21}, which may lead to undesirable mode coupling.

On breaking the inversion symmetry of photonic crystals that possess Dirac cones, a photonic band gap (PBG) around Dirac points may open up \cite{23}. With the presence of edges, edge states within the PBG may appear with a sharp confinement of optical fields at the edges \cite{24}. With further breaking of the time-reversal symmetry, confined edge states even become unidirectional, showing robustness against scattering or disorder \cite{7, 25-28}. In this paper, we show theoretically that edge states in honeycomb photonic crystals (HPCs) can be exploited in realizing wideband trapping of...
light. Since no metal is introduced, the optical loss should be much lower than those in metamaterial and plasmonic waveguides. Compared with photonic crystal waveguides, our system differs in being unimodal and is more compact as well. Although exemplified by HPCs with rods that are infinitely long, our idea can be applied to two-dimensional photonic crystals with finite rod lengths or membrane photonic crystals with drilled holes [20–22].

The HPCs under study consist of dielectric rods which are arranged in a honeycomb lattice in air, in analogy to graphene, as schematically shown in figure 1(a). The inter-distance between adjacent rods is denoted by \( d \). In an infinite HPC, there are two different sets of rods whose radii are denoted respectively by \( r_1 \) and \( r_2 \). The radius of the edge rods, which can be changed, is denoted by \( r_3 \). The lattice constant of an HPC is thus \( a = \sqrt{3}d \). Without loss of generality, the dielectric constant of all rods is taken to be 11.4, a typical value for silicon at telecommunication wavelengths.

In our following discussions, we only consider the transverse magnetic polarization, i.e., the case where the electric field is parallel to the rods.

In figure 1(c), photonic band structures of infinite HPCs, calculated by a plane-wave expansion method [4], are shown. For an HPC possessing inversion symmetry, i.e., \( r_1 = r_2 \), Dirac points exist where the first and second photonic bands cross each other at the K point with a reduced frequency of \( a/\lambda = 0.253 \). With broken inversion symmetry, i.e., \( r_1 \neq r_2 \), the degeneracy at the K point will be lifted and a PBG will open up [23]. The lower (upper) edge of the PBG is defined by the first (second) photonic band at the K (M) point.

To attain an HPC with an optimal or desired PBG, one can tune the radius of the rods or adjust the dielectric constant of the rods. In figure 1(d), the PBG map as a function of \( r_2 \) for fixed \( r_1 = 0.4d \) is shown. For \( r_1 = r_2 = 0.4d \), there is no PBG due to the existence of the Dirac points. For \( r_1 \neq r_2 \), a PBG always exists. For \( r_1 = 0.4d \) and \( r_2 = 0.2d \), the PBG ranges in reduced frequency \( a/\lambda \) from 0.26 to 0.343. For \( r_1 = 0.4d \) and \( r_2 = 0 \), the relative PBG width, \( \Delta \omega /\omega_m \), can be as high as 43%, where \( \Delta \omega \) is the PBG width and \( \omega_m \) is the mid-gap frequency.

Figure 2(a) shows the dispersion of edge states for an HPC with a zigzag edge, calculated by the plane-wave expansion method [4]. In our calculations, a supercell with a size of \( a \) along the edge direction and 46 \( d \) along the direction perpendicular to the edge direction is used. Periodic boundary conditions are imposed in both directions. The supercell contains a finite HPC with a thickness of 35\( d \) along the direction perpendicular to the edge direction, corresponding to 48 rows of rods including the edge rods. Since the separations of the two zigzag edges are large enough, there is no coupling between the two edges. The resulting dispersion can thus be considered as that for a single zigzag edge of a semi-infinite HPC. Projected photonic bands are obtained by projecting the bulk photonic band structure over the wavevector along the edge direction, \( k_1 \). In addition to photonic bands, for a given radius of the edge rods \( r_3 \), an edge state may appear between...
the first and second photonic bands. Interestingly, this edge state is unimodal; its dispersion depends on $r_3$.

Even for different values of $r_3$, the dispersions of the edge state show similar behavior: its frequency increases with increasing $k_\parallel$ up to the Brillouin zone boundary $k_\parallel = \pi/a$. At $k_\parallel = \pi/a$, it takes a zero slope. In other words, the group velocity decreases with increasing $k_\parallel$ and approaches zero at the Brillouin zone boundary. This interesting feature could be exploited to slow down and even stop light [14, 20]. The frequency of an edge state at $k_\parallel = \pi/a$ is dubbed the cutoff frequency since the frequencies of the edge state at other wavevectors are always smaller than the cutoff frequency. For different values of $r_3$, the corresponding cutoff frequency differs, showing a monotonic decrease with increasing $r_3$, as shown in the inset of figure 2(a).

Note that edge states lie below the light line, implying that they are evanescent waves. In figures 2(b)–(d), the field distributions for the edge state with $r_3 = 0.28d$ at different $k_\parallel$ are shown. Obviously, optical fields are confined to the edge rods. For the edge mode at $k_\parallel = 0.6\pi/a$, it is near the first photonic band, leading to some bulk excitations in the vicinity of the edge, which can be clearly seen from figure 2(b). In contrast, for the edge modes away from the photonic bands there are almost no bulk excitations. As shown by us [24], these edge modes are of subwavelength confinement, like surface plasmons bounded at metallic surfaces [29].

As aforementioned, an edge state at its cutoff frequency has a zero group velocity and the cutoff frequency decreases monotonically with increasing $r_3$. These features can yield wideband trapping of light by taking advantage of edge states, provided that the edge rods are designed to have a spatially graded variation in radius. If the grade is small enough, the graded edge can be considered approximately as a series of small edges, in each of which the edge rods possess a constant radius. As a result, each location seems to have a different cutoff frequency. For a wave propagating along such a graded edge, its group velocity will be gradually reduced along the edge direction and eventually approach zero at a location where the corresponding cutoff frequency coincides with the frequency of the wave. In other words, the wave will stop around this location.

Figure 3 shows light trapping for different frequencies at the graded zigzag edge of an HPC, simulated by a finite-difference time-domain (FDTD) method [30]. The radii of the edge rods are assumed to vary linearly with the position of the edge rods, namely, $r_3 = 0.3d + 5 \times 10^{-4}x$, where $x$ is the position along the edge direction. In our FDTD simulations, a continuous Gaussian beam with an intensity of 1 and a width of $2d$ is launched at $x = -46a$. Perfectly matched layer absorbing boundaries [31] are used.

Obviously, from figure 3 light beams of different frequency can be trapped spatially in different locations. The scenario is as follows. For a right-propagating Gaussian beam, the propagation will be rightwards after launching. The beam will be slowed down towards the right since its group velocity decreases rightwards due to the reduction of the radius of the edge rods. It will eventually be stopped around the location where the corresponding cutoff frequency of the location coincides with the beam frequency. By inspecting the beam with a reduced frequency of 0.286, for example, it is seen that the maximum intensity of the standstill beam occurs around the position $x \approx -4a$. The radius of the edge rods around this location is about 0.29$d$, very close to but a bit smaller than the radius of 0.3$d$ that offers a cutoff frequency of 0.286 (see the inset of figure 2(a)). For the standstill beam, there are some small additional peaks on the left side of the main peak. This is because the right-propagating wave may get reflected more or less since the grade of the edge rods causes, effectively, a variation in refractive index along the edge direction. The reflected and the right-propagating waves may interfere with each other, leading to these small additional peaks, which could be suppressed in principle by using a finer grade.

In summary, we studied theoretically the edge states at the zigzag edge of HPCs consisting of dielectric rods in air.
for transverse magnetic polarization. With broken inversion symmetry, a PBG exists between the first and second photonic bands. A unimodal edge state may appear within the PBG, whose dispersion and cutoff frequency can be tuned by changing the radius of the edge rods. For a zigzag edge with a gradually graded radius in the edge rods, light beams of different frequencies can be slowed down and trapped spatially in different locations. Our results show that edge states in HPCs could be exploited in optical storage and enhanced light–matter interactions.

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References

[1] Castro Neto A H, Guinea F, Peres N M R, Novoselov K S and Geim A K 2009 Rev. Mod. Phys. 81 109
[2] Yablonovitch E 1987 Phys. Rev. Lett. 58 2486
[3] John S 1987 Phys. Rev. Lett. 58 2486
[4] Joannopoulos J D, Johnson S G, Winn J N and Meade R D 2008 Photonic Crystals: Molding the Flow of Light 2nd edn (Princeton, NJ: Princeton University Press)
[5] Peleg O, Bartal G, Freedman B, Manela O, Segev M and Christodoulides D N 2007 Phys. Rev. Lett. 98 103901
[6] Sepkhanov R A, Bazalyy Ya B and Beenakker C W J 2007 Phys. Rev. A 75 063813
[7] Haldane F D M and Raghu S 2008 Phys. Rev. Lett. 100 013904
[8] Zhang X D 2008 Phys. Rev. Lett. 100 113903
[9] Han D Z, Lai Y, Z L, Zhang Z-Q and Chan C T 2009 Phys. Rev. Lett. 102 123904
[10] Benisty H 2009 Phys. Rev. B 79 155409
[11] Zandbergen S R and de Dood M J A 2010 Phys. Rev. Lett. 104 043903
[12] Huang X Q, Lai Y, Hang Z H, Zheng H H and Chan C T 2011 Nature Mater. 10 582
[13] Tsakmakidis K L, Boardman A D and Hess O 2007 Nature 450 397
[14] Vlasov Y A, O’Boyle M, Hamann H F and McNab S J 2005 Nature 438 65
[15] Zhao X P, Luo W, Huang J X, Fu Q H, Song K, Cheng X C and Luo C R 2009 Appl. Phys. Lett. 95 071111
[16] Stockman M I 2004 Phys. Rev. Lett. 93 137404
[17] Smolyaninova V N, Smolyaninov I I, Kildishev A V and Shalaev V M 2010 Appl. Phys. Lett. 96 211121
[18] Gan Q, Fu Z, Ding Y J and Bartoli F J 2008 Phys. Rev. Lett. 100 256803
[19] Gan Q, Gao Y, Wagner K, Vezhenov D, Ding D Y and Bartoli F J 2011 Proc. Natl Acad. Sci. 108 5169
[20] Gershen H, Karle T J, Engelen R J P, Bogaerts W, Korterik J P, van Hulst N F, Kraussn T F and Kuipers L 2005 Phys. Rev. Lett. 94 073903
[21] Krauss T F 2007 J. Phys. D: Appl. Phys. 40 2666
[22] Mori D and Baba T 2005 Opt. Express 13 9398
[23] Chong Y D, Wen X-G and Soljačić M 2008 Phys. Rev. B 77 235125
[24] Ouyang C, Xiong Z, Zhao F, Dong B, Hu X, Liu X and Z J 2011 Phys. Rev. A 84 015801
[25] Wang Z, Chong Y D, Joannopoulos J D and Soljačić M 2008 Phys. Rev. Lett. 100 013905
[26] Ochiai T 2010 J. Phys.: Condens. Matter 22 225502
[27] Fu J-X, Liu R-J and Li Z-Y 2010 Appl. Phys. Lett. 97 041112
[28] Poo Y, Wu R-X, Lin Z, Yang Y and Chan C T 2011 Phys. Rev. Lett. 106 093903
[29] Barnes W L, Dereux A and Ebbesen T W 2003 Nature 424 824
[30] Taflove A 1995 Computational Electrodynamics: The Finite Difference Time Domain Method (London: Artech House)
[31] Berenger J-P 1994 J. Comput. Phys. 114 185