Impact of Mismatch Angle on Electronic Transport Across Grain Boundaries and Interfaces in 2D Materials

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We study the impact of grain boundaries (GB) and misorientation angles between grains on electronic transport in 2-dimensional materials. Here we have developed a numerical model based on the first-principles electronic bandstructure calculations in conjunction with a method which computes electron transmission coefficients from simultaneous conservation of energy and momentum at the interface to essentially evaluate GB/interface resistance in a Landauer formalism. We find that the resistance across graphene GBs vary over a wide range depending on misorientation angles and type of GBs, starting from 53 Ω μm for low-mismatch angles in twin (symmetric) GBs to about 1020 Ω μm for 21° mismatch in tilt (asymmetric) GBs. On the other hand, misorientation angles have weak influence on the resistance across MoS2 GBs, ranging from about 130 Ω μm for low mismatch angles to about 6000 Ω μm for 21°.

The interface resistance across graphene-MoS2 heterojunctions also exhibits a strong dependence on misorientation angles with resistance values ranging from about 100 Ω μm for low-mismatch angles in Class-I (symmetric) interfaces to 1015 Ω μm for 14° mismatch in Class-II (asymmetric) interfaces. Overall, symmetric homo/heterojunctions exhibit a weak dependence on misorientation angles, while in MoS2 both symmetric and asymmetric GBs show a gradual dependence on mismatch angles.

Graphene, a monolayer of sp² hybridized carbon atoms arranged in a honeycomb lattice structure, has a unique Dirac cone electronic structure and exhibits numerous interesting properties including quasi-ballistic electron transport up to several microns of length even at room temperature. Besides graphene, transition metal dichalcogenides (TMDs) are another class of two-dimensional (2D) materials which have attracted intense research interests in recent years. The potential applications of graphene and TMDs have motivated mass scale production of large-area films. Among the most popular methods, chemical-vapor deposition (CVD) on transition metal substrates is relatively cheap and extensively used to grow high quality large two-dimensional sheets. However, CVD-grown films are typically found to be polycrystalline in nature, consisting of many single crystalline grains each with random crystal orientation and separated by grain boundaries (GBs). Several studies have reported that grain boundaries in 2D materials impact both their electronic and thermal properties.

The earliest of these studies focused on the electrical resistance across graphene GBs. Experimentally, graphene GB resistance has been found to vary over a broad range from a few Ω μm to tens of kΩ μm. Huang et al. showed a wide distribution of misorientation angles between adjacent grains in a polycrystalline monolayer graphene sheet with a preferential low angle growth of about 7°. The GB resistance across such GBs was found to be about 240 Ω μm. Contrasting this to the sheet resistance of 700 Ω/μm for the entire device, they concluded that the GB resistance is about one-third of the total resistance of a 250 nm grain. Koepke et al. observed a reduction in mobility in CVD-grown graphene and attributed it to the strong carrier scattering at grain boundaries. Clark et al. found resistance across graphene GBs to be varying between 40–140 Ω μm for samples with misorientation angles ranging from 9° to 21°. The resistivity of GBs was more than 3 times the bulk resistivity of the grains consistently across all of their samples. There was a positive correlation between misorientation angles and GB resistance, but the width of the transition region surrounding the GB also played a role.

Besides experimental measurements, there are several theoretical studies which have helped to gain more insight on transport across graphene GBs. Yazyev and Louie found that GBs across grains represented by the...
same translational vectors are highly transparent to charge carriers with a transmission of about 80%, whereas
GBs formed by grains with different translational vectors behave as perfect reflectors of carriers. Vancso et al.\textsuperscript{16}
performed wave packet dynamical transport calculations to show that transmission properties across graphene
GBs depend on misorientation angles as well as localized structures at the boundaries. Zhang et al.\textsuperscript{17} showed that
intrinsic (defect-free) GBs are almost transparent to carrier transport in highly symmetric GBs. They concluded
that the degradation in transmission mainly comes from the extrinsic defects at the boundaries which results in
the passivation of the $\pi$-orbital. Recently, Sun et al.\textsuperscript{18} investigated electrical properties along different transport
directions with respect to the GB direction using Density Functional Theory (DFT) calculations combined with
Green's function technique. They showed that the zero band gap nature of graphene bandstructure remains intact
even in the presence of GBs. They also found that there is an at least 50% current suppression in the transport
across GBs as compared to the current in pristine graphene. Despite the numerous studies on various types of
graphene GBs, the dependence of GB resistance on misorientation angles is still inconclusive.

There has also been a growing interest in electrical transport of CVD-grown MoS\textsubscript{2}\textsuperscript{20–23}; however, little is
known about the impact of misorientation angles on its GB resistance. Najmaei et al.\textsuperscript{20} studied the individual
and collective effect of GBs on electronic transport properties and found that the carrier mobility shows a weak
dependence on channel length up to 75 $\mu$m. Kang et al.\textsuperscript{24} also reported a similar dependence of field-effect mobility
on channel length, again indicating that GBs don't significantly degrade the electronic transport properties in
CVD-grown MoS\textsubscript{2}. This observation was further corroborated by Schmidt et al.\textsuperscript{25}, where they demonstrate that the
electronic properties of CVD-grown monolayer MoS\textsubscript{2} are comparable to those of their exfoliated counterparts.
In contrast, Ly et al.\textsuperscript{26} showed that MoS\textsubscript{2} sheets exhibit very poor electrical transport properties (mobilities
below 70 cm\textsuperscript{2} V\textsuperscript{-1} s\textsuperscript{-1}) for all their devices with different misorientation angles. They observed a positive but
non-linear correlation between field-effect mobility and misorientation angles.

Electronic transport in lateral\textsuperscript{26–28} as well as vertical\textsuperscript{30–32} 2D heterostructures has recently gained significant
research attention with particular focus on graphene-contacted MoS\textsubscript{2} lateral (in-plane) heterostructures\textsuperscript{30–36}. Graphene
has been reported to form an ohmic contact with MoS\textsubscript{2}\textsuperscript{26,37}, resulting in an increase in mobility up to an order of magnitude as compared to that of in metal-MoS\textsubscript{2} field-effect transistors (FETs). This calls for inves-
tigating the role of misorientation angles in determining the graphene-MoS\textsubscript{2} interface resistance in such hetero-
structures. Throughout the numerous studies of the resistance of GBs and interfaces, a common thread is that the
resistance spans a wide range of values depending on mismatch angle. A definitive trend explaining this variation, especially in MoS\textsubscript{2} GBs and graphene-MoS\textsubscript{2} interfaces, still requires further investigation.

In this paper, we focus on the fundamentals behind the impact of grain misorientation angles in 2D homo-
junctions and heterojunctions. Starting from electronic structure obtained through first principles Density
Functional Theory (DFT), we calculate the transmission coefficients and boundary/interface resistances for
graphene and MoS\textsubscript{2} grain boundaries, as well as graphene-MoS\textsubscript{2} heterojunctions. We use the transmission coeffi-
cients to compute the conductance of the boundaries/interfaces as a function of both mismatch angle and carrier
concentration. In Sec. 2 we further detail our approach and delineate two different classes of GBs (twin and tilt homo-
junctions) and interfaces (Class-I and II heterojunctions). In Sec. 3, we discuss our results showing that
transport across twin homojunctions and Class-I heterojunctions show a weak dependence on mismatch angles,
whereas the resistance across tilt homojunctions and Class-II heterojunctions exhibits a strong dependence on
mismatch angles. We conclude in Sec. 4 that GBs play a moderate role in MoS\textsubscript{2} due to its parabolic bands, but can be
quite significant in graphene and large-mismatch graphene-MoS\textsubscript{2} heterostructures owing to graphene's steep
linear Dirac cones.

Theoretical approach

To study the impact of misorientation angles on interface resistance, we have developed a numerical model based on
first-principles DFT electronic bandstructure calculations and electron transmission coefficients from simul-
taneous energy and momentum conservation. The latter is an extension of the approach originally proposed by
Yazyev and Louie\textsuperscript{38} to calculate the transmission coefficient of electrons across a graphene grain boundary.
The interface resistance is calculated in the following steps: bandstructure calculations for graphene and MoS\textsubscript{2}
individually from the first principles, rotation of the Brillouin zones (BZ) to account for the misorientation angle
between adjacent grains, calculation of electron transmission across the interface from the energy and momen-
tum conservation, and finally computing the interface resistance in the Landauer formalism. For heterojunctions
between dissimilar materials, an additional second step involves band alignment at the interface based on the
Schottky-Mott rule.

First, we calculate the electronic bandstructure for single-layer graphene and MoS\textsubscript{2} individually from first
principles using Density Functional Theory (DFT) as implemented within the open-source distribution Quantum
Espresso\textsuperscript{39} (further details on the DFT calculations are given in the Methods). It is followed by the alignment of
the bands at the interface. In homojunctions such as graphene-graphene GBs and MoS\textsubscript{2}-MoS\textsubscript{2} GBs, the bands are
always well-aligned at the interface, whereas in heterojunctions, such as the graphene-MoS\textsubscript{2} GBs, the bands need
to be aligned. In contrast to the planar charge in a 3D interface, a 2D heterojunction forms a line dipole at the
junction\textsuperscript{39}. It has been shown that in 2D heterojunctions, the effect of the interfacial dipole vanishes when the
overall dimensions of the device are much larger than the characteristic junction-width, typically about 10 nm\textsuperscript{39}.

As a result, the band alignment in 2D heterojunctions is far less sensitive to the interfacial details and the band
alignment closely follows the Schottky-Mott rule\textsuperscript{39}.

In our case, the graphene and MoS\textsubscript{2} are treated as semi-infinite, so we use the Schottky-Mott rule\textsuperscript{40} and align
the vacuum levels of the two materials at the interface. Next, the work function of graphene ($\phi_{\text{graphene}}=4.55$ eV\textsuperscript{41}$)
and the electron affinity of MoS\textsubscript{2} ($\chi_{\text{MoS}_2}=4.2$ eV\textsuperscript{42}$) are used to align the respective bands away from the interface
relative to the vacuum level. Due to the difference in the work function of graphene and electron affinity of MoS\textsubscript{2},
an energy barrier \( \Phi_{BC} = \phi_{\text{graphene}} - \chi_{\text{MoS}_2} \) is formed at the interface. As graphene is essentially metallic, the bands bend on the MoS\(_2\) side near the interface to account for the energy barrier height in equilibrium. The amount of band-bending on MoS\(_2\) side, which is also a function of carrier concentration \( n_\text{C} \), is given by

\[
\Phi_{BC} = -\phi_{\text{MoS}_2} (n_\text{C}) - \chi_{\text{MoS}_2} - \Phi_{\text{graphene}} (n_\text{C}).
\]

The carrier concentration typically depends on the level of impurities, doping, or gating\(^{43-45}\).

The orientation of the grains with respect to the GB/interface is defined by two angles \( \Theta_L \) and \( \Theta_R \), each being the angle of rotation between the grain on the left and the right side with respect to the interface, taken here as reference, as shown in Fig. 1. According to our convention, \( \Theta_L \) is taken to be positive for anticlockwise rotation of the left grain, whereas \( \Theta_R \) is positive for clockwise rotation of the right grain. We define misorientation angle as \( \Theta_M = \Theta_L + \Theta_R \). To include the effect of the misorientation angle in our calculation, the wavevectors in the first Brillouin zone are rotated by \( \Theta_L \) for the left grain and \( \Theta_R \) for the grain on the right hand side of the interface. The rotation of the Brillouin zone does not affect the aforementioned band structure alignment at the interface.

In 2D materials, GBs can be of different types depending on both the orientation of each grain with respect to the grain boundary and the orientation of the grains with respect to each other. One extreme is when both the grains are rotated symmetrically by equal angles away from the GB in opposite directions (i.e. \( \Theta_L = \Theta_R = \Theta_M/2 \)) and the second is when only one of the grains is rotated away from the interface (i.e. \( \Theta_L = 0^\circ \), \( \Theta_R = \Theta_M \)). In literature, the former type of symmetric grain boundaries are referred to as twin GBs and the latter as the most asymmetric tilt GBs.

So far, we have discussed the two extreme cases of GBs for a given misorientation angle \( \Theta_M \), but we can have many intermediate cases of tilt (asymmetric) GBs depending on the position of the boundary itself. For example, given that \( \Theta_M = 4^\circ \) we can have \( \Theta_L = \Theta_R = \Theta_M/2 \) (twin GBs), or \( \Theta_L = 0^\circ \) and \( \Theta_R = \Theta_M \) (the most asymmetric tilt GB), or intermediate cases such as \( \Theta_L = 1^\circ \) and \( \Theta_R = 3^\circ \), and so on and so forth. In order to denote these intermediate tilt cases, we introduce an angle \( \Theta_B \) which is defined as the angle, in the anticlockwise direction, that the boundary makes with the reference line. So, an intermediate case of \( \Theta_M = 4^\circ \) and \( \Theta_B = 1^\circ \).

The effect of GB/interface on transport is incorporated by using boundary conditions based on quantum-mechanical wave continuity\(^{46}\). From translational symmetry, transmission requires simultaneous conservation of energy and transverse momentum of the incident electron across the interface. Momentum conservation requires that the parallel component of the incident wave vector \( k_i \) be equal to the parallel component of the transmitted wave vector \( k_t \) in their respective domains that is \( k_{\parallel i} = k_{\parallel t} \); simultaneously, energy is conserved.
by finding a perpendicular component of the transmitted wave vector \( k_{t} \), within the first Brillouin zone of the right grain, such that \( E_{t}(k_{u} + k_{t}) = E_{t}(k_{t}) = E_{i}(k_{t} + k_{u}) \). Then we calculate the mode-dependent transmission coefficient \( \tau_{b}(k) \) for each band \( b \) using the perpendicular components of the incident \( k_{i} \) and transmitted \( k_{t} \) wave vectors by the expression

\[
\tau_{b}(k) = \left| \frac{4k_{u} \cdot k_{t}}{k_{i} + k_{u}} \right|^{2}
\]

(1)

Next, we obtain the energy-resolved transmission coefficient \( \Gamma_{b}(E) \) by averaging the mode-dependent transmission coefficient \( \tau_{b}(k) \) over the constant energy contour, described by \( \delta(E - E_{i}(k)) \), using the 2D version of the linear extrapolation approach described by Gilat and Rauhberger as

\[
\Gamma_{b}(E) = \frac{1}{4\pi^{2}} \int \tau_{b}(k) \delta(E - E_{i}(k)) dk
\]

(2)

The denominator of Eq. 2 is the density of states in band \( b \) \( D_{b}(E) \), shown in Fig. 1(b). The same transformation method is employed for converting the mode-dependent velocity \( v_{b}(k) \) into energy-resolved velocity \( v_{b}(E) \) in the direction of transport. We then calculate the transport distribution function TDF \( \Xi(E) \) as

\[
\Xi(E) = \sum_{b} v_{b}(E) \Gamma_{b}(E) D_{b}(E)
\]

(3)

The TDF is then used to numerically calculate the grain boundary conductance in the Landauer formalism and inverted to obtain the grain boundary resistance \( R_{GB/int} \). The grain boundary conductance is obtained from an integral of the product of TDF and Fermi window function \( \frac{\partial f(E - E_{F}, T)}{\partial E} \) over energy

\[
G_{GB/int} = \frac{e^{2}}{2} \int_{E_{C}}^{E_{max}} \Xi(E) \left| \frac{\partial f(E - E_{F}, T)}{\partial E} \right| dE
\]

(4)

where \( E_{C} \) is the bottom of the conduction band and \( E_{max} \) is the highest electron energy in the first four conduction bands and \( f(E) \) is the Fermi-Dirac distribution function \( f(E) = [1 + \exp((E - E_{F})/k_{B}T)]^{-1} \).

**Results and Discussion**

**Electron transport across graphene grain boundaries.** We calculate the transmission and resistance of graphene GBs in order to explore the impact of the misorientation angle. The angle dependence of GB resistance largely depends on the type (tilt or twin) of the GB. Figure 2(a,b) show transmission coefficient \( \Gamma(E) \) and GB resistance \( R_{GB} \) respectively for various misorientation angles in twin GBs. We see in Fig. 2(a) that perfect transmission, that is transmission coefficient \( \Gamma(E) \) equals 1, is obtained for 0° mismatch angle at any given energy level. However, as the misorientation angle increases, the modes that do not conserve energy and transverse momentum are reflected at the interface, resulting in a reduction of the transmission coefficient, which varies between 0.8 and 0.5 for various mismatch angles. Besides band gap, the energy range for which there is no transmission (\( \Gamma(E) = 0 \)) is referred here as transmission/transport gap. In twin GBs, we note that even for large mismatch angles there is no transmission gap in the energy spectrum.

For GBs with 0° mismatch angle, we obtain a coefficient \( \Gamma(E) = 1 \); in contrast, Yazeyev and Louie reported a linear transmission probability \( \Gamma(E) \) with energy. They used a non-equilibrium Green’s function (NEGF) formalism to calculate conductance across graphene grain boundaries. In the coherent transport regime, the conductance from NEGF formalism reduces to the conductance in Landauer formalism, given by \( G = \frac{e^{2}}{2} \int \Xi(E) \left| \frac{\partial f(E - E_{F}, T)}{\partial E} \right| dE \).

Comparing this with our conductance expression (Eq. 4), we find that \( \Xi(E) \) in the NEGF formalism is analogous to our transport distribution function \( \Xi(E) \). For the graphene GBs with 0° mismatch, \( \Xi(E) \) in Eq. 3 is proportional to the DOS \( D_{b}(E) \), which is linear with energy [as shown in Fig. 1(b) and Eq. 8]; thus our TDF is consistent with the \( T(E) \) vs. energy plot from NEGF.

In Fig. 2(b), the GB resistance is plotted for different misorientation angles and carrier concentrations. For a given carrier concentration, the GB resistance increases with misorientation angles. This is due to the reduction in transmission coefficient with increasing misorientation angle, as can be seen in Fig. 2(a), which maps to an increase in GB resistance. Perfect transmission at 0° mismatch angle translates into ballistic resistance across graphene GBs as shown in Fig. 8(b) in the Appendix [same as the blue curve in Fig. 2(b)]. For a given mismatch angle, the GB resistance decreases with increasing carrier concentration as we can see in Fig. 2(b). At intrinsic carrier concentration, the Fermi level \( E_{F} \) is near the Dirac point in graphene. But with the increase in electron concentration the Fermi level goes into the conduction band, and consequently, the Fermi window function \( (−df/dE) \) which is centered at \( E_{F} \) also shifts towards higher energy levels. As the DOS in graphene is proportional to energy near the Dirac point (from Eq. 8 and Fig. 2(b)), the TDF \( \Xi(E) \) also increases with energy away from the Dirac point. Thus the value of the integral in Eq. 4, which is a product of TDF and Fermi window function, increases with carrier concentration. As a result, we see a decrease in GB resistance with increasing carrier concentration in Fig. 2(b).

Figure 2(c,d) show transmission coefficient \( \Gamma(E) \) and grain boundary resistance respectively for various mismatch angles in tilt grain boundaries. The transmission coefficient shows a similar reduction with increasing
mismatch angles as seen in Fig. 2(a); however, the reduction is more pronounced than in the case of twin GBs. In tilt GBs we also observe a widening of the transmission gap, shown in the Fig. 2(c), with increasing misorientation angle. This transmission gap around the Dirac point maps into large GB resistance for large-angle tilt GBs and grain boundary resistance becomes less sensitive to the variation in carrier concentration.

Previously, it was found that the GB resistance across graphene GBs varies within a wide range from a few $\Omega \mu m$ to several $k\Omega \mu m^{3,4}$. The wide variation in GB resistance can be fully explained with the trends observed in Fig. 2(b,d): there is a large difference in resistance between twin and tilt GBs, with twin GBs being less sensitive to misorientation angles as compared to the tilt GBs. The GB resistance in tilt GBs range from about $350 \Omega \mu m$ at $4^\circ$ mismatch to several thousands of $G\Omega \mu m$ at $14^\circ$ mismatch, even at high carrier concentration of about $10^{13} \text{ cm}^{-2}$. The transmission coefficient eventually becomes zero for misorientation angles beyond $14^\circ$ mismatch due to the large transmission gap in tilt GBs and we observe extremely high values of resistances. In contrast, the resistance of twin GBs in near-intrinsic graphene varies from $400 \Omega \mu m$ at low to about $1 k\Omega \mu m$ at high mismatch angles, while at high carrier concentration it varies over a very narrow range of about $90 \Omega \mu m$ at $4^\circ$ mismatch to $110 \Omega \mu m$ at $14^\circ$ mismatch. Our calculated graphene GB resistances include a ballistic resistance of $53 \Omega \mu m$ at high carrier concentration of $10^{13} \text{ cm}^{-2}$ and $424 \Omega \mu m$ at intrinsic carrier concentration. After removing the ballistic resistance, the calculated GB resistance for a low-mismatch twin GBs of about $1^\circ$ at high carrier concentration is $8 \Omega \mu m$. This is in good agreement with Grosse et al.$^{11}$.

**Electron transport across MoS$_2$ grain boundaries.** To study electronic resistance across MoS$_2$ GBs, we use the same procedure as used for graphene GBs in the previous section. The transmission coefficient as a function of energy is plotted in Fig. 3(a) for different misorientation angles in twin GBs. The blue curve shows transmission across an imaginary, perfectly-matched grain boundary (which corresponds to $0^\circ$ mismatch). A perfect transmission is obtained for energies greater than about $0.94 \text{ eV}$ and less than about $-0.94 \text{ eV}$. Zero transmission at energies between $-0.94 \text{ eV}$ and $0.94 \text{ eV}$ corresponds to the energy band gap of $1.88 \text{ eV}$ in intrinsic MoS$_2$. We also observe a gradual reduction in transmission coefficient with increasing misorientation angles as compared to that of graphene GBs. However, there is no transmission gap found for MoS$_2$ twin GBs, similar to what we observed in graphene twin GBs. Corresponding to the transmission coefficient for various misorientation angles, the boundary resistance across MoS$_2$ twin grain boundaries vs. carrier concentration is shown in Fig. 3(b). We note that the values of $R_{GB}$ in MoS$_2$ twin GBs are almost double than the values of GB resistance in graphene twin

![Figure 2](image-url)
boundaries for a carrier concentration of $1 \times 10^{12}$ cm$^{-2}$, whereas for large carrier concentrations between $6 \times 10^{12}$ and $9 \times 10^{12}$ cm$^{-2}$, MoS$_2$ twin GBs have GB resistance similar to that of graphene twin GBs.

Figure 3(c,d) show transmission coefficient vs. energy and GB resistance vs. carrier concentration respectively for various misorientation angles in MoS$_2$ tilt GBs. It can be seen in Fig. 3(c) that the transmission coefficient decreases with increasing misorientation angle and the rate of reduction of transmission coefficient is more rapid than what was observed in MoS$_2$ twin GBs. Like in tilt graphene GBs, a transmission gap is also observed in tilt MoS$_2$ GBs for large misorientation angles, however the transmission gap in MoS$_2$ is much smaller than that of graphene. We attribute this trend to the flatter parabolic conduction band bottom of MoS$_2$ as compared to the steep conical bandstructure of graphene around the Dirac point. The variation of GB resistance with misorientation angle is quite distinct in this case as compared to the variation of $\Gamma_{GB}$ in graphene tilt GBs. It is important to note that the resistance across MoS$_2$ GBs is much smaller than what we found in graphene tilt GBs. Thus, misorientation of adjacent grains across grain boundaries can cause a significant reduction in electronic conductance in polycrystalline graphene, while GBs in polycrystalline MoS$_2$ might not play such a strong role in electron conduction, which is in good agreement with few recent reports on electronic transport in CVD-grown MoS$_2$.

Figure 4(a,b) depict the surface plots of GB resistance vs. $\Theta_M$ and $\Theta_B$ for graphene and MoS$_2$ GBs respectively. The calculated value of resistances across graphene GBs range from few tens of $\Omega \mu$m to about $10^{13}$ $\Omega \mu$m depending on the $\Theta_M$ (the angle between the two grains) and $\Theta_B$ (the position of the boundary with respect to the left grain). However, the GB resistance across MoS$_2$ GBs vary over a relatively narrow range of about $130 \Omega \mu$m to $5700 \Omega \mu$m for various combinations of $\Theta_M$ and $\Theta_B$. Thus, we can see that for a given misorientation angle, one can have different GB resistance depending on the position of the GB with respect to the grains, and any resistance value falling in this range can be explained by a combination $\Theta_M$ and $\Theta_B$.

Electron transport across graphene-MoS$_2$ interfaces. The interfaces formed between two dissimilar materials (heterojunctions) are different from those of homojunctions because of the difference in the properties of the grains on either side of the interface—including electron affinity, work function, and bandstructure. So, before discussing about electron transport across such heterojunctions, we redefine the nomenclature of the interfaces formed between graphene and MoS$_2$ to differentiate with those of homojunctions. When graphene (taken here to be on left side of the boundary) and MoS$_2$ (right side of the boundary) grains are rotated by equal angles with respect to the interface i.e. $\Theta_g = \Theta_R$, we use the term Class-I interface, whereas when $\Theta_g \neq \Theta_R$ we call them Class-II interfaces in this work.
Figure 5(a) shows the thermionic transmission of the electrons across graphene-MoS$_2$ Class-I interface for various misorientation angles at a carrier concentration of $1 \times 10^{12}$ cm$^{-2}$. Due to the difference in the work function and electron affinity in graphene and MoS$_2$, the bands bend and an energy barrier (the energy difference between fermi-level, approximately equal to 0 eV in Fig. 5(a,c), to the bottom of the conduction band of MoS$_2$ at the interface where the transmission of electrons start) is formed at the interface. Like in homojunctions, the band alignment at the interface is independent of the misorientation angle, and thus, the barrier height is also independent of $\Theta_M$. In Fig. 5(b), we see that at low carrier concentrations of about $1 \times 10^{12}$ cm$^{-2}$, the interface resistance is in the order of $10^8$ $\Omega \mu$m because of the large energy barrier. However, at high carrier concentrations between $6 \times 10^{12}$ cm$^{-2}$ and $9 \times 10^{12}$ cm$^{-2}$, the interface resistance reduces significantly because the energy barrier between graphene and MoS$_2$ almost disappears at such concentrations and they behave like Ohmic contacts.

Figure 5(c) shows transmission coefficient vs. energy for various misorientation angles in Class-II graphene-MoS$_2$ interfaces at a carrier concentration of $1 \times 10^{12}$ cm$^{-2}$. The transmission coefficient decreases with increasing mismatch angle similar to the tilt GBs in graphene GBs. A transmission gap is formed in addition to the existing potential barrier, marked in the figure, and this transmission gap widens with increasing misorientation angles. Transmission becomes zero for large mismatch angles beyond 14°. This strong dependence of mismatch angle on transmission coefficient leads to a strong dependence of the interface resistance on misorientation angles in Class-II graphene-MoS$_2$ heterojunctions, which can be seen in Fig. 5(d). At a carrier concentration of $1 \times 10^{12}$ cm$^{-2}$, the interface resistance varies from about $10^8$ for low mismatch angles to $10^{14}$ $\Omega \mu$m for a mismatch of 14°, whereas at high concentrations the interface resistance ranges from about $10^6$ for low mismatch angles to $10^8$ $\Omega \mu$m for a mismatch of 14°.

In homojunctions like graphene-graphene and MoS$_2$-MoS$_2$ GBs, the band alignment is independent of the position of the Fermi level so the transmission coefficient is also independent of carrier concentration. In contrast, the barrier height in heterojunctions is a function of carrier concentration via the position of the Fermi level, owing to the difference in DOS between graphene and MoS$_2$. The transmission coefficient in Class-I graphene-MoS$_2$ interface is plotted with carrier concentration in Fig. 6. Figure 6(a) shows the transmission coefficient vs. energy for perfectly matched graphene-MoS$_2$ interface, that is 0° mismatch. The shape of the $\Gamma(E)$ vs. energy does not change with carrier concentration rather the curves get shifted towards the left in energy due to the decrease in energy barrier height with carrier concentration. In Fig. 6(b,c), the transmission coefficient vs. energy is plotted for 4° mismatch in Class I and II heterojunctions respectively. The decrease in the magnitude of transmission coefficient as compared to that of Fig. 6(a) is more pronounced for Class II than Class-I interfaces. For large misorientation angles, that is beyond 14° the transmission coefficient in Class II interfaces becomes very small about 0.1 eV as can be seen in Fig. 6(d), whereas for Class I heterojunctions the transmission coefficient

Figure 4. Shows resistance (a) across graphene GBs and (b) across MoS$_2$ GBs vs. misorientation angles $\Theta_M$ and various combinations of $\Theta_L$ and $\Theta_R$, represented as $\Theta_B$ for a given $\Theta_M$. Here $\Theta_B$ is expressed as a fraction of $\Theta_M$. 
peak is about 0.4 eV (shown by the green curve in Fig. 5(a), noting that a change in carrier concentration only shifts the $\Gamma$ vs E curve and does not change the shape).

Figure 7 shows a comparison of the interface resistance among Gr-Gr, MoS$_2$-MoS$_2$, and Gr-MoS$_2$ interfaces. It can be seen that, in general, symmetric twin GBs in homojunctions and Class-I interfaces in heterojunctions show a very weak dependence on the degree of mismatch between adjacent grains, whereas tilt GBs in homojunctions and Class-II interfaces in heterojunctions exhibit strong dependence on misorientation angles except in MoS$_2$, where both tilt and twin GBs are found to show a weak dependence on mismatch angles. The weak angle dependence in MoS$_2$-MoS$_2$ GBs can be attributed to the flat parabolic conduction band because of which the underlap in the bandstructures on the either side of the GB is quite small even at large mismatch angles. In order to explain the wide range of the graphene GB resistances in the literature via misorientation angle and type of GBs, the data from the literature has also been included in the figure. The yellow markers in the figure denote the combinations of $\Theta_M$ and $\Theta_B$ obtained by fitting the experimental measurements by Kochat et al. 50 ($\Theta_B = 2.83^\circ$ for $\Theta_M = 12^\circ$, and $\Theta_B = 3^\circ$ for $\Theta_M = 22^\circ$ respectively), Clark et al. 14 ($\Theta_B = 0^\circ$, $0.2^\circ$, and $0.75^\circ$ for $\Theta_M = 9^\circ$, $14^\circ$, and $21^\circ$ respectively), and Yu et al. 3 ($\Theta_B = 3.1^\circ$ for $\Theta_M = 28^\circ$).

The aim of our study is to understand the effect of misorientation angle on GB conductance. There could be additional effects due to grain boundary roughness 9 and the presence of localized electronic states, which have been observed at 3D interfaces 51 and 2D grain boundaries 25,52,53. The localized states are not included in our model, but could be treated by modifying $D_b(E)$ in Eq. 3. The presence of localized interface states could lead to two types of behavior, depending on the magnitude of the transport gap. For low mismatch angles or symmetric GBs where the transport gap is small and the transmission coefficient is close to unity, the localized states and roughness at the GB would reduce the transmission coefficient; in that case, our calculated conductance values can be thought of as an upper bound. For large mismatch angles, we found a wide transport gap where transmission is zero, especially in graphene GBs and graphene-MoS$_2$ interfaces. Then localized states might introduce additional channels for transmission and lead to slightly higher GB conductance than what we report here without these localized states. In that sense, our conductance values could be thought of as a lower bound.

Figure 5. (a) Shows transmission coefficient vs. energy for various misorientation angles across graphene-MoS$_2$ Class-I interfaces. (b) Shows the variation of interface resistance with carrier concentration for the same mismatch angles as plotted in (a). Class-I graphene-MoS$_2$ interfaces show negligible sensitivity towards misorientation angles. (c) Shows transmission coefficient vs. energy for different misorientation angles in graphene-MoS$_2$ Class-II interfaces. On top of intrinsic barrier height, an additional transmission gap opens up for such Class-II graphene-MoS$_2$ interfaces. The resulting interface resistance in Class-II interfaces vs. carrier concentration for different misorientation angles are plotted in (d).
Figure 6. Show transmission coefficient vs. energy for various carrier densities (a) for 0° mismatch, (b,c) for 4° in Class-I and Class-II graphene-MoS$_2$ interfaces respectively, and (d) for 14° mismatch in Class II interfaces.

Figure 7. Compares the calculated GB/interface resistance vs. misorientation angles across twin (solid lines) and tilt (dashed lines) Gr-Gr (shown in blue) and MoS$_2$-MoS$_2$ (shown in magenta) GBs, and Class-I (solid black line) and Class-II (dashed black line) Gr-MoS$_2$ interfaces. The reported values of graphene GB resistance in the literature are also plotted in this figure. The data for graphene GB resistance which are available with misorientation angles are plotted with blue markers. The other studies about graphene GB resistance where mismatch angle wasn’t mentioned explicitly are plotted on the right with red and black markers. The red markers are the resistance values from literature across single graphene GB. The black markers are for the literature data on GB resistance extracted by polycrystalline scaling from polycrystalline samples. The yellow markers represent the calculated graphene GB resistance corresponding to those combinations of $\Theta_M$ and $\Theta_B$ which fit the experimental measurements.
Conclusion
In conclusion, we find that misorientation angle between two adjacent grains plays a very significant role in both homojunctions and heterojunctions. We show that the resistance across graphene GBs and graphene-MoS$_2$ interfaces varies over a very wide range depending on the degree of mismatch between adjacent grains and type of GBs. The transmission coefficient across symmetric interfaces (twin GBs in homojunctions and Class-I interfaces in heterojunctions) is found to be less sensitive to misorientation angles between adjacent grains because they deflect electrons rather coherently. In these symmetric interfaces, there is no transmission gap. On the other hand, the transmission across asymmetric interfaces (tilt GBs in homojunctions and Class-II interfaces in heterojunctions) is largely diminished by mismatch angles and a transmission gap opens up in the energy spectrum. In contrast to graphene-graphene tilt GBs, the resistance across MoS$_2$-MoS$_2$ tilt GBs show relatively much weaker dependence on mismatch angles. This is attributed to the flat parabolic conduction band bottom in MoS$_2$ compared to the steep conical conduction band bottom in graphene. As a result, the rotation of the BZ in MoS$_2$ by large angles causes a small transmission gap, whereas even a small misorientation angle across graphene GBs gives rise to a large transmission gap. In homojunctions, the bands are identical on either side of the interface and the response to the carrier concentration, and hence the back-gated voltage, is also uniform on both sides. Thus, for a given misorientation angle, the variation of transmission coefficient vs. energy is independent of carrier concentration in homojunctions. In heterojunctions, the bands are aligned at the interface using the macroscopic variables, including work function and electron affinity, based on Schottky-Mott rule, forming an energy barrier at the interface. The band alignment, and with it the energy barrier between graphene and MoS$_2$, reduces with the carrier concentration because of the differences in their densities-of-states. Consequently, the interface resistance strongly decreases with carrier concentration in heterojunctions in both classes of interfaces. In summary, electrical transport across twin homojunctions and Class-I heterojunctions shows a weak dependence on mismatch angles, whereas the resistance across tilt homojunctions and Class-II heterojunctions exhibits a strong dependence on mismatch angles.

Methods
Density Functional Theory calculations of the electronic bandstructure. For graphene, we used a scalar relativistic, norm-conserving pseudopotential (NCPP) which implements a direct-fit Von Barth-Car method with a Perdew-Zunger local density approximation (LDA) exchange-correlation functional. For MoS$_2$, we used a nonrelativistic NCPP for Mo and a scalar relativistic NCPP for S. Both potentials employed a Martins-Troullier method with a Perdew-Wang LDA exchange correlation. The lattice constants are $a = 2.459$ Å for graphene and $a = 3.125$ Å, $z = 3.11$ Å for MoS$_2$, where $z$ is the distance between chalcogen atoms. To ensure that interplanar interactions are neglected, the repeating images of the monolayers are separated by a $20$ Å vacuum. The cutoff energy for plane waves was $120$ Ry for graphene and $140$ Ry for MoS$_2$. We used a convergence threshold of $10^{-13}$ on a Monkhorst-Pack grid sizes of $8 \times 8 \times 1$ for graphene and $6 \times 6 \times 4$ for MoS$_2$ for the initial total energy calculation and then performed a bandstructure calculation on a dense grid of $25,208$ k-points (wavevectors) with a convergence threshold of $10^{-12}$. We used the central difference method to obtain the electron velocities per band which, in turn, are subsequently used in calculating the electronic density of states (DOS) and other transport properties including interfacial transmission and resistance of the interface.

Appendix: Ballistic resistance of graphene-graphene interface. We derive an analytical expression for the ballistic resistance across graphene GBs and compare it with the numerically computed values of ballistic resistance at different carrier concentrations. We define ballistic resistance as the resistance between two perfectly-matched grains, that is when misorientation angle ($\Theta_m$) is $0^\circ$. In the diffusive limit (Ohmic regime)
when the dimension of the conductor is large compared to the carrier mean free path, the conductance varies inversely with length. One would expect the conductance to become infinite when the conductor length tends to zero. However, it has been experimentally found in both metals and semiconductors that the measured conductance converge to a finite value called ballistic conductance. The regime where we see this limiting behavior is called ballistic regime. In this regime, characterized by an absence of scattering, the conductor has no resistance—the ballistic resistance is not the resistance of the conductor but the contact resistance.

With a careful treatment of the voltage across the GB, as done in a 4-probe measurement and analogous to the corrections made to the temperature gradient for phonon transmission, one could remove the ballistic contact resistance and show that the resistance across an idealized perfectly-matched GB is zero. In our calculations, the GB resistance at any given mismatch angle includes the ballistic resistance, which varies with the carrier concentration. So, while comparing the 4-probe experimental measurements of GB resistance for a given mismatch, we subtract the ballistic resistance from the calculated GB resistance.

The ballistic conductance for 1D conductor is given by the expression \( G_{\text{ball,1D}} = G_{\text{ball,1D}} \times M_{2D}(E_F) \) (5)

The channel number at any energy \( E \) for a given width of the ribbon is calculated as \( M(E) = W \frac{h}{4} \langle v_F(E) \rangle D_{2D}(E) \) (6)

where \( \langle v_F(E) \rangle \) is calculated by 2D averaging of velocity of all the modes, \( \langle v_F(E) \rangle = \frac{1}{E} v_F \), \( v_F \) is the Fermi velocity \((\approx 10^6 \text{ m s}^{-1})\), which is computed from the slope of the bandstructure \((E-k)\) relationship around Dirac point. \( D_{2D}(E) \) is the 2D density of states.

The dispersion of graphene around the Dirac point is approximated by the relation \( E(k) = \hbar v_F |k| \) where \( \hbar \) is the reduced Planck’s constant. The general expression for calculating 2D density of states is

\[
D_{2D}(k) = \frac{1}{2\pi^2} \frac{2\pi |k|}{\nabla E(k)} g_s g_v
\]

(7)

where \( g_s \) and \( g_v \) are constants related to the spin of electron and valley degeneracy respectively. For graphene \( g_v = 2 \) and \( g_s = 2 \) for electrons. \( \nabla E(k) \) is the gradient of energy dispersion with respect to the wavevector and around the Dirac point it can be approximated by \( hv_F \). Thus for graphene,

\[
D_{2D}(E) = \frac{2}{\pi \hbar^2 v_F^2} |E|
\]

(8)

In general, 2D carrier concentration is given as

\[
n_{2D}(E_F) = \int_0^\infty f_0(E) D_{2D}(E) dE
\]

(9)

where \( f_0(E) \) is the equilibrium Fermi-Dirac distribution function, \( f_0(E) = \left[ 1 + \exp\left(\frac{E-E_F}{k_B T}\right) \right]^{-1} \). As graphene is degenerate, so Eq. 9 can be approximated by

\[
n_{2D}(E_F) = \int_0^{E_F} D_{2D}(E) dE = \int_0^{E_F} \frac{2}{\pi \hbar^2 v_F^2} E dE = \frac{E_F^2}{\pi \hbar^2 v_F^2}
\]

(10)

Using the expressions for density of states and 2D-averaged velocity, channel number in Eq. 6 for graphene can be written as

\[
M_{2D}(E_F) = \frac{2}{\pi \hbar v_F} \frac{E_F}{W}
\]

(11)

Replacing the expression for channel number obtained from Eq. 11 in Eq. 5, we can calculate ballistic conductance in graphene as

\[
\frac{G_{\text{ball,2D}}}{W} = \frac{8 q^2}{h^2 v_F} \frac{E_F}{W}
\]

(12)

From Eqs 10 and 12, ballistic conductance in graphene can be expressed in terms of carrier concentration as

\[
\frac{G_{\text{ball,2D}}}{W} = \frac{4 q^2}{h} \frac{\sqrt{M_{2D}}}{\pi}
\]

(13)
Thus the ballistic resistance $R_{\text{ball}}$ in graphene, which is the reciprocal of $G_{\text{ball}}$, is inversely proportional to the square root of carrier concentration. On using the values of the constants in Eq. 13 and intrinsic carrier concentration of $8 \times 10^{10}$ cm$^{-2}$, the analytical value of $R_{\text{ball}}$ in graphene is about 405 $\Omega$. We compare these analytically calculated values of ballistic resistance for different carrier concentrations with our numerically calculated values as shown in Fig. 8(b). At intrinsic carrier concentration ($n_i = 8 \times 10^{10}$ cm$^{-2}$), the numerically calculated ballistic resistance is 424 $\Omega$, which compares quite well with the analytical value of 405 $\Omega$. In Fig. 8(a) we can see that transmission coefficient $\Gamma(E)$ is 1 for the entire energy range, showing perfect transmission for 0° mismatch (perfectly-matched grains). The curve encompassing the blue area in the figure is the Fermi window function, which is defined as the derivative of Fermi-Dirac distribution function with perfect transmission for 0° mismatch (perfectly-matched grains).

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Author Contributions
Z.A. conceived the idea and supervised the work. A.K.M. performed band alignment and conductance calculations. C.J.F. performed the first principles DFT calculations. A.K.M. and C.J.F. conducted the transmission calculations. All authors reviewed the manuscript.

Additional Information
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