The effect of composite resonances on Higgs decay into two photons

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Abstract In scenarios of strongly coupled electroweak symmetry breaking, heavy composite particles of different spin and parity may arise and cause observable effects on signals that appear at loop levels. The recently observed process of Higgs to $\gamma\gamma$ at the LHC is one of such signals. We study the new constraints that are imposed on composite models from $H \rightarrow \gamma\gamma$, together with the existing constraints from the high precision electroweak tests. We use an effective chiral Lagrangian to describe the effective theory that contains the Standard Model spectrum and the extra composites below the electroweak scale. Considering the effective theory cutoff at $\Lambda = 4\pi v \sim 3$ TeV, consistency with the $T$ and $S$ parameters and the newly observed $H \rightarrow \gamma\gamma$ can be found for a rather restricted range of masses of vector and axial-vector composites from 1.5 to 1.7 and 1.8 to 1.9 TeV, respectively, and only provided a non-standard kinetic mixing between the $W^3$ and $B^0$ fields is included.

1 Introduction

One of the possible signals of composite Higgs boson models is the deviation of the $h \rightarrow \gamma\gamma$ channel from the Standard Model (SM) prediction, as it is a loop process sensitive to heavier virtual states. For instance this signal was predicted in the context of Minimal Walking Technicolor [1]. Consequently the recent $h \rightarrow \gamma\gamma$ signal reported by ATLAS and CMS collaborations [2–5], which is very close to the SM prediction, implies an additional constraint on composite models. In this regard, it is important to explore the consequences of this new constraint on composite models, in conjunction with those previously known from electroweak precision measurements.

Given the recent evidence of the Higgs boson, a strongly interacting sector that is phenomenologically viable nowadays should include this scalar boson in its low energy spectrum, but it is also assumed that vector and axial-vector resonances should appear as well, in a way that the so called Weinberg sum rules [6] are satisfied [7–9].

Here we formulate this kind of scenario in a general way, without referring to the details of the underlying strong dynamics, by using a low energy effective Lagrangian which incorporates vector and axial-vector resonances, as well as composite scalars. One of these scalars should be the observed Higgs and the others should be heavier as to avoid detection at the LHC. Our inclusion of the vector and axial resonances is based on a 4-site Hidden Local Symmetry, which requires three scalar sectors (link fields) responsible for the breaking of the hidden local symmetries. This setup naturally leads to a spectrum that contains three physical scalars.

The main reason to still consider strongly interacting mechanisms of electroweak symmetry breaking (EWSB) as alternatives to the Standard Model mechanism is the so called hierarchy problem that arises from the Higgs sector of the SM. This problem is indicative that, in a natural scenario, new physics should appear at scales not much higher than the EWSB scale (say, around a few TeV) in order to stabilize the Higgs mass at scales much lower than the Planck scale ($\sim 10^{19}$ GeV). An underlying strongly interacting dynamics without fundamental scalars, which becomes non-perturbative somewhere above the EW scale, is a possible scenario that gives an answer to this problem. The strong dynamics causes the breakdown of the electroweak symmetry through the formation of condensates in the vacuum [10–16].

Many models of strong EWSB have been proposed which predict the existence of composite particles such as scalars [17–48], vectors [49–62], both scalars and vectors [63–79], and composite fermions [80,81]. These predicted scalar and vector resonances play a very important role in preserving
the unitarity of longitudinal gauge boson scattering up to the cutoff \( \Lambda \simeq 4\pi v \) [56,82–88]. One should add that a composite scalar does not have the hierarchy problem since quantum corrections to its mass are cut off at the compositeness scale, which is assumed to be much lower than the Planck scale.

In this work we assume a scenario where there is a strongly interacting sector which possesses a global \( SU(2)_L \times SU(2)_R \) symmetry. The strong dynamics spontaneously breaks this global symmetry down to its diagonal \( SU(2)_{L+R} \) subgroup. As the electroweak gauge group is assumed to be contained in the \( SU(2)_L \times SU(2)_R \) symmetry, the breaking of this symmetry down to the \( SU(2)_{L+R} \) subgroup is in fact the realization of electroweak symmetry breaking. Consequently, the interactions among the Standard Model particles and all extra composite resonances can be described by an effective chiral Lagrangian where the \( SU(2)_{L+R} \) is non-linearly realized. The explicit \( SU(2)_{L+R} \) that remains plays the role of a custodial symmetry of the strong sector.

Just as in the SM, the custodial symmetry is explicitly broken by the hypercharge coupling \( g' \) and by the difference between up- and down-type quark Yukawa couplings. The strong dynamics responsible for EWSB in our scenario gives rise to composite massive vector and axial vector fields \( V^a_\mu \) and \( A^a_\mu \), respectively belonging to the triplet representation of the \( SU(2)_{L+R} \) custodial group, as well as two composite scalars \( (h) \) and one pseudoscalar \( (\eta) \), all singlets under that group. We will identify the lightest scalar, \( h \), with the state of mass \( m_h = 126 \) GeV discovered at the LHC. All of these composite resonances are assumed to be lighter than the cutoff \( \Lambda \simeq 4\pi v \), so that they explicitly appear as fields in the effective chiral Lagrangian. Composite states of spin 2 and higher are assumed to be heavier than the cutoff, and so they are disregarded in this work.

These composite particles are important signatures of the strongly coupled scenarios of EWSB and they could manifest themselves either by direct production or as virtual states in loop corrections. The lack of direct observation of these particles at the LHC or any previous collider is expected if their masses are large enough, but their loop effects may still be detectable. In this work we study two types of quantities where loop effects are important: the corrections to the oblique parameters \( S \) and \( T \) [89–94] and the decay rate \( h \to \gamma\gamma \). Specifically, we use the high precision results on \( S \) and \( T \) and the recent ATLAS and CMS results at the LHC on \( h \to \gamma\gamma \) to constrain the mass and coupling parameters of the model. The rate \( h \to \gamma\gamma \) is particularly important in our study as it is a one-loop process which is sensitive to the existence of extra vector and axial-vector particles. In this sense, we are studying whether composite models are viable alternatives to electroweak symmetry breaking, given the current experimental success of the Standard Model [95].

Besides the presence of the heavy vectors, another feature of composite scenarios is that the fermion masses may not be exactly proportional to the scalar–fermion couplings as in the SM. In particular, we found coupling of the Higgs to top quarks to be slightly larger than what is obtained in the SM through a Yukawa term.

The organization of the paper is as follows. In Sect. 2 we introduce our effective Lagrangian that describes the spectrum of the theory. In Sect. 3 we describe the calculations of our quantities of interest, i.e. the \( T \) and \( S \) oblique parameters and the rate \( h \to \gamma\gamma \), within our model. In Sect. 4 we study numerically the constraints on the model parameters, mainly masses and couplings of the extra composite fields, in order to be consistent with the high precision measurements as well as the two-photon signal recently observed in the LHC experiments. Finally in Sect. 5 we state our conclusions.

2 The effective chiral Lagrangian with spin-0 and spin-1 fields

In this work we formulate our strongly coupled sector by means of an effective chiral Lagrangian that incorporates the heavy composite states by means of local hidden symmetries [96]. As shown in Appendix A and described in detail in Ref. [56], this Lagrangian is based on the symmetry \( \Gamma = SU(2)_L \times SU(2)_C \times SU(2)_D \times SU(2)_R \). The \( SU(2)_C \times SU(2)_D \) part is a hidden local symmetry whose gauge bosons are linear combinations of the vector and axial-vector composites, and the SM gauge fields [cf. Eq. (A.21)]. The SM gauge group, on the other hand, is contained as a local form of the \( SU(2)_L \times SU(2)_R \) global symmetry of the underlying dynamics.

As the symmetry \( \Gamma \) is spontaneously broken down to the diagonal subgroup \( SU(2)_{L+C+D+R} \), it is realized in a non-linear way with the inclusion of three link fields (spin-0 multiplets). These link fields contain two physical scalars \( h \) and \( H \), one physical pseudoscalar \( \eta \), the three would-be Goldstone bosons absorbed as longitudinal modes of the SM gauge fields and the six would-be Goldstone bosons absorbed by the composite triplets \( V_\mu \) and \( A_\mu \).

The starting point is the lowest order chiral Lagrangian for the \( SU(2)_L \times SU(2)_R \) Goldstone fields, with the addition of the invariant kinetic terms for the \( W \) and \( B \) bosons:

\[
\mathcal{L}_\chi = \frac{v^2}{4} \left( D_\mu U D^{\mu} U^\dagger \right) - \frac{1}{2g^2} \left( W_{\mu\nu} W^{\mu\nu} \right) - \frac{1}{2g'^2} \left( B_{\mu\nu} B^{\mu\nu} \right) + \frac{c_{WB}}{4} \left( U^\dagger W_{\mu\nu} U B^{\mu\nu} \right). \tag{2.1}
\]

Here \( \langle \rangle \) denotes the trace over the \( 2 \times 2 \) matrices, while \( U \) is the matrix that contains the SM Goldstone boson fields \( \pi^a \) \((a = 1, 2, 3)\) after the symmetry is spontaneously broken. \( U \) transforms under \( SU(2)_L \times SU(2)_R \) as \( U \to g_R U g_L^T \) and can be expressed as

\[ g_R U g_L^T = g_R \Lambda(t) g_L^T, \]
\[ U = e^{i\pi^a \tau^a}, \]  
(2.2)

where \( \tau^a \) the Pauli matrices. \( D_\mu U \) is the covariant derivative with respect to the SM gauge transformations:

\[ D_\mu U = \partial_\mu U - i B_\mu U + i U W_\mu, \]  
(2.3)

and \( W_{\mu\nu} \) and \( B_{\mu\nu} \) are the matrix form of the SM tensor fields, respectively,

\[
W_{\mu\nu} = \partial_\mu W_\nu - \partial_\nu W_\mu - i \left[ W_\mu, W_\nu \right],
\]

\[
B_{\mu\nu} = \partial_\mu B_\nu - \partial_\nu B_\mu.
\]
(2.4)

where \( W_\mu = g W_\mu^a \tau^a/\sqrt{2} \) and \( B_\mu = g B_\mu^a \tau^3/\sqrt{2} \) are the gauge boson fields in matrix form. Note that we added a kinetic mixing term \( W^3 - B^0 \), proportional to a (so far arbitrary) coupling \( c_{WB} \).

The vector and axial-vector composite fields formed due to the underlying strong dynamics are denoted here as \( V_\mu = V_\mu^a \tau^a/\sqrt{2} \) and \( A_\mu = A_\mu^a \tau^3/\sqrt{2} \), respectively. They are assumed to be triplets under the unbroken \( SU(2)_L + R \) symmetry.

Their kinetic and mass terms in the effective Lagrangian can be written as

\[ L_{V}^{\text{kin}} = -\frac{1}{4} \langle V_{\mu\nu} V^{\mu\nu} \rangle + \frac{1}{2} M_V^2 \langle V_\mu V^\mu \rangle, \]  
(2.5)

\[ L_{A}^{\text{kin}} = -\frac{1}{4} \langle A_{\mu\nu} A^{\mu\nu} \rangle + \frac{1}{2} M_A^2 \langle A_\mu A^\mu \rangle. \]  
(2.6)

Here the tensor fields \( V_{\mu\nu} = \nabla_\mu V_\nu - \nabla_\nu V_\mu \) and \( A_{\mu\nu} = \nabla_\mu A_\nu - \nabla_\nu A_\mu \) are written in terms of a covariant derivative in order to include the electroweak gauge symmetry embedded in \( SU(2)_L \times SU(2)_R \) [56]:

\[
\nabla_\mu V_\nu = \partial_\mu V_\nu + \left[ \Gamma_\mu, V_\nu \right],
\]

\[
\nabla_\mu A_\nu = \partial_\mu A_\nu + \left[ \Gamma_\mu, A_\nu \right],
\]  
(2.7)

where the connection \( \Gamma_\mu \) satisfies \( \Gamma_\mu = -\Gamma_\mu \) and is given by

\[ \Gamma_\mu = \frac{1}{2} \left[ u^\dagger (\partial_\mu - i B_\mu) u + u (\partial_\mu - i W_\mu) u^\dagger \right], \]

with \( u \equiv \sqrt{U} \).
(2.8)

Assuming that the underlying strong dynamics is invariant under parity, the composite fields \( V_\mu \) and \( A_\mu \) can be included in the effective Lagrangian as combinations of gauge vectors of a hidden symmetry, also spontaneously broken. In that formulation further interaction terms appear in the effective Lagrangian, as derived in Appendix A. The terms that contain one power of \( V_\mu \) or \( A_\mu \), according to Eq. (A.32), are given by

\[
L_{1V} = -\frac{f_V}{2\sqrt{2}} \left( V^{\mu\nu} \left( u W_{\mu\nu} u^\dagger + u^\dagger B_{\mu\nu} u \right) \right)
-\frac{i g_V}{2\sqrt{2}} \left( V^{\mu\nu} \left[ u_\mu, u_\nu \right] \right)
-\frac{i k f_A}{2\sqrt{2}} \left( \left( \partial_\mu u_\nu - \partial_\nu u_\mu + [\Gamma_\mu, u_\nu] - [\Gamma_\nu, u_\mu] \right) \left[ V^\mu, u_\nu^\dagger \right] \right),
\]  
(2.9)

\[
L_{1A} = \frac{f_A}{2\sqrt{2}} \left( \left( \partial_\mu u_\nu - \partial_\nu u_\mu + [\Gamma_\mu, u_\nu] - [\Gamma_\nu, u_\mu] \right) A^{\mu\nu} \right)
-\frac{i f_A}{2\sqrt{2}} \left( u W_{\mu\nu} u^\dagger + u^\dagger B_{\mu\nu} u \right) \left[ A^\mu, u_\nu^\dagger \right],
\]  
(2.10)

where \( u_\mu = u_\mu^\dagger = i u^\dagger D_\mu U u^\dagger \) is a quantity that transforms covariantly under \( SU(2)_L + R \). For later convenience we have also redefined the couplings in terms of the dimensionless quantities \( f_V, g_V, \) and \( f_A \) [see Eqs. (A.32) and (A.38)], which depend on the masses of \( V_\mu \) and \( A_\mu \), according to

\[ f_V \equiv \frac{1}{g_c} \sqrt{\frac{1}{1 - k M_V}}, \quad g_V = \frac{1 - k^2}{2} f_V, \quad f_A = -k f_V, \]  
(2.11)

where \( k = M_V^2 / M_A^2 \) [see Eq. (A.38)]. In this way, the interactions of the vector fields \( V_\mu \) with two longitudinal weak bosons are characterized by the coupling \( g_V \), while the interactions of \( V_\mu \) with one longitudinal and one transverse gauge boson are characterized by both \( g_V \) and \( f_V \). In turn, the interactions of the axial-vector fields \( A_\mu \) with one longitudinal and one transverse gauge boson are characterized by the coupling \( f_A \). Finally, the mixing of \( V_\mu \) and of \( A_\mu \) with the SM gauge fields are proportional to \( g f_V \) and \( g f_A \), respectively.

Now, the terms with two powers of \( V_\mu \) and \( A_\mu \), as shown in Appendix A, are

\[
L_{2V} = -\frac{1 - k^2}{8} \left( [V_\mu, V_\nu] \left[ u^\mu, u^\nu \right] \right)
+\frac{\kappa^2}{8} \left( [V_\mu, u_\nu] \left( [V^\mu, u^\nu] - [V^\nu, u^\mu] \right) \right)
+\frac{i}{4} \left( [V^\mu, V^\nu] \left( u W_{\mu\nu} u^\dagger + u^\dagger B_{\mu\nu} u \right) \right),
\]  
(2.12)

\[
L_{2A} = -\frac{1 - k^2}{8} \left( [A_\mu, A_\nu] \left[ u^\mu, u^\nu \right] \right)
+\frac{\kappa^2}{8} \left( [A_\mu, u_\nu] \left( [A^\mu, u^\nu] - [A^\nu, u^\mu] \right) \right)
+\frac{i}{4} \left( [A^\mu, A^\nu] \left( u W_{\mu\nu} u^\dagger + u^\dagger B_{\mu\nu} u \right) \right),
\]  
(2.13)

\[
L_{1V,1A} = -\frac{i \kappa}{2} \left( V_{\mu\nu} \left[ A^\mu, u^\nu \right] \right)
-\frac{i \kappa}{2} \left( A_{\mu\nu} \left[ V^\mu, u^\nu \right] \right)
-\frac{i k}{2} \left( \partial_\mu u_\nu - \partial_\nu u_\mu + [\Gamma_\mu, u_\nu] - [\Gamma_\nu, u_\mu] \right) \left[ V^\mu, u^\dagger \right] \times \left[ V^\mu, A^\nu \right],
\]  
(2.14)
The terms with three powers of $V_\mu$ and $A_\mu$, also derived in Appendix A and included in Eq. (A.32), are

$$\mathcal{L}_{3V} = \frac{i g_C}{\sqrt{2}} [V^{\mu\nu} [V_\mu, V_\nu]].$$

(2.15)

$$\mathcal{L}_{3A} = -\frac{\kappa g_C}{\sqrt{2}} [ \{A_\mu, A_\nu\} [A^\mu, u^\nu] ],$$

(2.16)

$$\mathcal{L}_{V.2A} = \frac{i g_C}{\sqrt{2}} (V_{\mu\nu} [A^\mu, A^\nu]) + \frac{i g_C}{\sqrt{2}} (A_{\mu\nu} [V^\mu, A^\nu]),$$

(2.17)

$$\mathcal{L}_{A.2V} = -\frac{\kappa g_C}{\sqrt{2}} ( [V_\mu, V_\nu] [A^\mu, u^\nu])$$

$$-\frac{\kappa g_C}{\sqrt{2}} ( [V_\mu, u_\nu] ( [V^\mu, A^\nu] - [V^\nu, A^\mu])).$$

(2.18)

The interactions given in (2.15)–(2.18) are controlled by the dimensionless parameter $g_C$, which is the coupling constant of the hidden local symmetry $SU(2)_C$ and $SU(2)_D$. In particular, $\mathcal{L}_{3V}$ describes the cubic self-interactions of $V_\mu$. Notice that, since $g_C = 1/f_V$ [cf. Eq. (2.11)], these self-interactions are strong when the mixings between the heavy vectors and the SM gauge bosons [cf. Eqs. (2.9, 2.10)] are weak.

Continuing with the expansion given in Eq. (A.32), the quartic self-interactions of $V_\mu$ and of $A_\mu$ are proportional to $g_C^2$ and described by the terms

$$\mathcal{L}_{4V} = \frac{g_C^2}{8} ( [V_\mu, V_\nu] [V^\mu, V^\nu]),$$

(2.19)

$$\mathcal{L}_{4A} = \frac{g_C^2}{8} ( [A_\mu, A_\nu] [A^\mu, A^\nu]).$$

(2.20)

$$\mathcal{L}_{2V.2A} = \frac{g_C^2}{4} ( [V_\mu, A_\nu] ( [V^\mu, A^\nu] - [V^\nu, A^\mu])$$

$$+ \frac{g_C^2}{4} ( [V_\mu, V_\nu] [A^\mu, A^\nu]).$$

(2.21)

Since $V_\mu^a$ and $A_\mu^a$ are linear combinations of the gauge bosons of the hidden local symmetry $SU(2)_C \times SU(2)_D$ and of the SM gauge fields [see Eq. (A.21)], the field strength tensors corresponding to the gauge bosons of this hidden local symmetry will include the field strength tensors of $V_\mu^a$ and $A_\mu^a$ as well as those of the SM gauge bosons [cf. Eqs. (A.23, A.24)]. Because of this reason, additional contact interactions involving the SM gauge fields and Goldstone bosons having couplings depending on $f_V, f_A$, and $g_V$ (see Eq. (2.11)) will automatically emerge from the invariant kinetic terms for the gauge bosons of the $SU(2)_C \times SU(2)_D$ sector. These contact interactions are given by

$$\mathcal{L}_{\text{contact}} = -\frac{f_V^2}{8} \left( \frac{1}{\beta} (\partial_\nu V_\mu - \partial_\mu V_\nu) + \frac{1}{\beta} (\partial_\nu A_\mu - \partial_\mu A_\nu) \right)$$

$$\times \left( \partial_\nu V_\mu - \partial_\mu V_\nu + \frac{1}{\beta} (\partial_\nu A_\mu - \partial_\mu A_\nu) \right)$$

$$+ \frac{g_V^2}{8} ( [u_\mu, u_\nu] [u_\mu, u_\nu])$$

$$- \frac{f_V^2}{8} \left( u_\mu u_\nu u^\nu + u^\nu u_\mu u_\nu \right)$$

$$- \frac{i f_V g_V}{4} \left( [u_\mu, u_\nu] (u_\mu u_\nu u^\nu + u^\nu u_\mu u_\nu) \right),$$

(2.22)

and they ensure that the scattering amplitudes involving SM particles have good behavior at high energies. For example, as shown in Ref. [71], the second term in Eq. (2.22), which contains four derivative terms involving only the SM Goldstone bosons, is crucial for having a consistent description of high energy WW scattering.

In addition to $V_\mu$ and $A_\mu$, there are two composite scalar singlets, $h$ and $H$, and one pseudoscalar singlet, $\eta$. We will identify the lightest of these fields, $h$, with the $m = 126$ GeV boson recently discovered at the LHC. The kinetic and mass terms for these spin-0 fields, as well as their interaction terms with one power in $h$, $H$ or $\eta$, are derived in Eqs. (A.4), (A.34), (A.37), and (A.38) of Appendix A, and they are given by

$$\mathcal{L}_h = \frac{1}{2} \partial_\mu h \partial^\mu h + m_h^2 h^2 - \frac{g_C^2}{2 \sqrt{2} (1 - \kappa)} h [V_\mu V^\mu]$$

$$+ \frac{g_C^2}{4} \left( \frac{1}{\sqrt{\beta}} - \frac{1}{2 \sqrt{1 - \kappa}} \right) v h [A_\mu A^\mu]$$

$$+ \frac{[2 \kappa \frac{1}{\sqrt{\beta}} -(1 - \kappa) \frac{1}{\sqrt{1 - \kappa}}]}{4 \sqrt{2}} v h [u_\mu u^\mu],$$

(2.23)

$$\mathcal{L}_H = \frac{1}{2} \partial_\mu H \partial^\mu H + m_H^2 H^2 + \frac{g_C^2}{2 \sqrt{2} (1 - \kappa)} H [V_\mu V^\mu]$$

$$+ \frac{g_C^2}{4} \left( \frac{1}{\sqrt{\beta}} - \frac{1}{2 \sqrt{1 - \kappa}} \right) v H [A_\mu A^\mu]$$

$$+ \frac{[2 \kappa \frac{1}{\sqrt{\beta}} +(1 - \kappa) \frac{1}{\sqrt{1 - \kappa}}]}{4 \sqrt{2}} v H [u_\mu u^\mu],$$

(2.24)

$$\mathcal{L}_\eta = \frac{1}{2} \partial_\mu \eta \partial^\mu \eta + \frac{m_\eta^2}{2} \eta^2 + \frac{g_C^2}{\sqrt{1 - \kappa}} [V_\mu A^\mu] \eta$$

$$+ \frac{g_C \sqrt{1 - \kappa} v}{\sqrt{2}} [V_\mu u^\mu] \eta.$$
\[ \mathcal{L}_{2h} = \frac{g_2^2}{16} h^2 \langle V_{\mu} V^{\mu} \rangle + \frac{5 g_2^2}{8} h^2 \langle A_{\mu} A^{\mu} \rangle + \frac{1}{32} \left( (1 - \kappa)^2 + 4 \kappa^2 \right) h^2 \langle u_\mu u^{\mu} \rangle + \frac{g_C (1 - 5 \kappa)}{8 \sqrt{2}} h^2 \langle A_{\mu} u^{\mu} \rangle, \]  
\[ \mathcal{L}_{2H} = \frac{g_2^2}{8} H^2 \langle V_{\mu} V^{\mu} \rangle + \frac{2 g_2^2}{8} H^2 \langle A_{\mu} A^{\mu} \rangle + \frac{1}{32} \left( (1 - \kappa)^2 + 4 \kappa^2 \right) H^2 \langle u_\mu u^{\mu} \rangle + \frac{g_C (1 - 5 \kappa)}{8 \sqrt{2}} H^2 \langle A_{\mu} u^{\mu} \rangle, \]  
\[ \mathcal{L}_{2\eta} = \frac{g_2^2}{8} \eta^2 \langle V_{\mu} V^{\mu} \rangle + \frac{2 g_2^2}{8} \eta^2 \langle A_{\mu} A^{\mu} \rangle + \frac{(1 - \kappa)^2}{16} \eta^2 \langle u_\mu u^{\mu} \rangle + \frac{g_C (1 - \kappa)}{4 \sqrt{2}} \eta^2 \langle A_{\mu} u^{\mu} \rangle, \]  
\[ \mathcal{L}_{hH} = \frac{g_2^2}{8} h H \langle V_{\mu} V^{\mu} \rangle + \frac{3 g_2^2}{8} h H \langle A_{\mu} A^{\mu} \rangle + \frac{4 \kappa^2 - (1 - \kappa)^2}{16} h H \langle u_\mu u^{\mu} \rangle - \frac{g_C (1 + 3 \kappa)}{4 \sqrt{2}} h H \langle A_{\mu} u^{\mu} \rangle, \]  
\[ \mathcal{L}_{h\eta} = - \frac{g_2^2}{2 \sqrt{2}} \langle V_{\mu} A^{\mu} \rangle h \eta - \frac{(1 - \kappa)}{4} g_C \langle V_{\mu} u^{\mu} \rangle h \eta, \]  
\[ \mathcal{L}_{H\eta} = \frac{g_2^2}{2 \sqrt{2}} \langle V_{\mu} A^{\mu} \rangle H \eta + \frac{(1 - \kappa)}{4} g_C \langle V_{\mu} u^{\mu} \rangle H \eta. \]  

Finally, we also consider the fermion mass and Yukawa terms:

\[ \mathcal{L}_Y = - \frac{v}{\sqrt{2}} \sum_{i, j} \left( \bar{u}_L^{(i)} d_L^{(j)} \right) U \left( 1 + a_{Eff} \frac{h}{v} + a_{Hff} \frac{H}{v} \right) \left( \lambda_i^u \lambda_j^d \eta \right) + h.c., \]  

where \( \lambda_i^u \) and \( \lambda_i^d \) are the up- and down-type quarks Yukawa couplings, respectively. Here \( a_{Eff} \) parametrizes in our model a deviation factor from the SM Higgs–fermion coupling (in the SM this factor is unity).

Since \( V_{\mu} \), \( h \), and \( H \) contribute to the elastic \( WW \) scattering amplitude, a good asymptotic behavior of the latter at high energies will depend on the \( a_{WW}, a_{HWW}, \) and \( g_Y \) parameters. Because of the extra contributions of \( H \) and \( V_{\mu} \), \( a_{WW} \) will turn out to be different from unity, in contrast to the SM.

Summarizing, in the framework of strongly interacting dynamics for EWSB, the interactions below the EWSB scale among the SM particles and the extra composites can be described by the effective Lagrangian:

\[ \mathcal{L}_{\text{eff}} = \mathcal{L}_X + \mathcal{L}_{\text{kin}} + \mathcal{L}_{\text{kin}} + \mathcal{L}_{1V} + \mathcal{L}_{2V} + \mathcal{L}_{2A} + \mathcal{L}_{1V, 1A} + \mathcal{L}_{1V, 2V} + \mathcal{L}_{A, 2V} + \mathcal{L}_{A, 2V} + \mathcal{L}_{\text{contact}} + \mathcal{L}_{hH} + \mathcal{L}_{hH} + \mathcal{L}_{hH} + \mathcal{L}_{V}, \]  

Our effective theory is based on the following assumptions:

1. The Lagrangian responsible for EWSB has an underlying strong dynamics with a global SU(2) \( \times \) SU(2) symmetry which is spontaneously broken by the strong dynamics down to the SU(2)_{L+R} custodial group. The SM electroweak gauge symmetry SU(2)L \( \times \) U(1)Y is assumed to be embedded as a local part of the SU(2)_{L+R} symmetry. Thus the spontaneous breaking of SU(2)_L \( \times \) SU(2)_{R} also leads to the breaking of the electroweak gauge symmetry down to U(1)_em.

2. The strong dynamics produces composite heavy vector fields \( V_{\mu} \) and axial-vector fields \( A_{\mu} \), triplets under the custodial SU(2)_{L+R}, as well as a composite scalar singlet \( h \) with mass \( m_h = 126 \text{ GeV} \), a heavier scalar singlet \( H \), and a heavier pseudoscalar singlet \( \eta \). These fields are assumed to be the only composites lighter than the symmetry breaking cutoff \( \Lambda \simeq 4 \pi v \).

3. The heavy fields \( V_{\mu} \) and \( A_{\mu} \) couple to SM fermions only through their kinetic mixings with the SM gauge bosons.

4. The spin-0 fields \( h \), \( H \), and \( \eta \) interacts with the fermions only via (proto)-Yukawa couplings.

Our Lagrangian has in total eight extra free parameters: the modified kinetic \( W^3-B^0 \) mixing coupling \( c_{WB} \), the scalar top quark couplings \( a_{htt}, a_{htt} \), the pseudoscalar top quark coupling \( a_{htt} \), the heavy vector and heavy axial-vector masses \( M_V \) and \( M_A \), and the heavy scalar and heavy pseudoscalar masses \( M_H \) and \( m_H \). However, from the expressions in Appendix B we can see that the oblique \( T \) and \( S \) parameters have little sensitivity to the masses of \( H \) and \( \eta \). Therefore, taking into account the experimental bound 600 GeV \( \lesssim m_H, m_H \lesssim 1 \text{ TeV} \) for heavy spin-0 particles, we can constrain the couplings of the heavy \( H \) and \( \eta \) to the top quark, \( a_{htt} \) and \( a_{htt} \), that enter in the radiative corrections to the masses of \( H \) and \( \eta \). We are then left with six free parameters: \( c_{WB}, a_{htt}, a_{htt}, a_{htt}, M_V \), and \( M_A \). In what follows, we will constrain these parameters by setting the mass \( m_h \) at 125.5 GeV (the recently discovered Higgs at the LHC), imposing the aforementioned experimental bound on \( m_H \) and \( m_H \), and imposing consistency with the high precision results on the \( T \) and \( S \) parameters and the current ATLAS and CMS results on the \( h \to \gamma \gamma \) rate.
3 Calculations of the rate $h \rightarrow \gamma \gamma$, the parameters $T$ and $S$ and the masses of $h$, $H$, and $\eta$

In the Standard Model, the $h \rightarrow \gamma \gamma$ decay is dominated by $W$ loop diagrams which can interfere destructively with the sub-dominant top quark loop. In our strongly coupled model, the $h \rightarrow \gamma \gamma$ decay receives additional contributions from loops with charged $V_{\mu}$ and $A_{\mu}$, as shown in Fig. 1. The explicit form for the $h \rightarrow \gamma \gamma$ decay rate is:

$$
\Gamma(h \rightarrow \gamma \gamma) = \frac{\alpha_{em}^2 m_h^3}{256\pi^3 v^2} \sum_f a_{hff} N_c Q_f^2 F_{1/2}(\beta_f) + a_{hVW} F_1(\beta_W) + a_{hVV} F_1(\beta_V) + a_{hAA} F_1(\beta_A),
$$

where

$$
a_{hWV} = \frac{2\kappa^2 - (1-\kappa)^2}{2\sqrt{2}}, \quad a_{hVV} = \frac{(1-\kappa)^2}{2\sqrt{2}}, \quad a_{hAA} = \kappa \left(1 - 2\sqrt{\frac{1-\kappa}{\kappa}}\right) a_{hVV}.
$$

Here $\beta_i$ are the mass ratios $\beta_i = m_i^2/M_i^2$, with $M_i = m_f, M_W, M_V$ and $M_A$, respectively, $\alpha_{em}$ is the fine structure constant, $N_C$ is the color factor ($N_C = 1$ for leptons, $N_C = 3$ for quarks), and $Q_f$ is the electric charge of the fermion in the loop. We should recall that $\kappa = M_V^2/M_A^2$ and $M_V = g_C v/\sqrt{1-\kappa}$, as shown in Eq. (A.38). From the fermion-loop contributions we will keep only the dominant term, which is the one involving the top quark.

The dimensionless loop factors $F_{1/2}(\beta)$ and $F_1(\beta)$ (for particles of spin-1/2 and spin-1 in the loop, respectively) are [97–104]:

$$
F_{1/2}(\beta) = 2[\beta + (\beta - 1) f(\beta)]\beta^{-2}, \quad (3.3)
$$

$$
F_1(\beta) = -\left[2\beta^2 + 3\beta + 3(\beta - 1) f(\beta)\right] \beta^{-2}, \quad (3.4)
$$

with

$$
f(\beta) = \begin{cases} 
\arcsin^2 \sqrt{\beta}, & \text{for } \beta \leq 1 \\
\frac{-1}{4} \left[\ln \left(\frac{1+\sqrt{1-\beta^{-1}}}{1-\sqrt{1-\beta^{-1}}}\right) - i\pi\right]^2, & \text{for } \beta > 1.
\end{cases}
$$

(3.5)

From the previous expressions it follows that the contribution of heavy vectors to $h \rightarrow \gamma \gamma$ strongly dominates over that of axial vectors when $M_V \ll M_A$, since in this case we have $a_{hVV} \gg a_{hAA}$.

Notice that we have not considered the contribution from contact interactions of gluons, such as

$$
L_{ggVV} = \frac{a_{ggVV}}{\Lambda^2} G_{\mu\nu} G^{\mu\nu} V_a V^a.
$$

(3.6)

to the Higgs production mechanism at the LHC, $gg \rightarrow h$, which could have a sizable effect that might contradict the current experiments. Nevertheless, we have checked that this contribution is negligible provided the effective coupling $a_{ggVV} < 0.5$. We recall that the heavy vector and heavy axial-vector resonances are colorless, and therefore they do not have renormalizable interactions with gluons.

Here we want to determine the range of values for $M_V$ and $M_A$ which is consistent with the $h \rightarrow \gamma \gamma$ results at the LHC. To this end, we will introduce the ratio $R_{\gamma\gamma}$, which normalises the $\gamma\gamma$ signal predicted by our model relative to that of the SM:

$$
R_{\gamma\gamma} = \frac{\sigma(pp \rightarrow h) \Gamma(h \rightarrow \gamma\gamma)}{\sigma(pp \rightarrow h)_{SM} \Gamma(h \rightarrow \gamma\gamma)_{SM}} \simeq a_{hV}^2 \frac{\Gamma(h \rightarrow \gamma\gamma)}{\Gamma(h \rightarrow \gamma\gamma)_{SM}}.
$$

(3.7)
This normalization for $h \rightarrow \gamma \gamma$ was also done in Ref. [105]. Here we have used the fact that in our model, single Higgs production is also dominated by gluon fusion as in the Standard Model.

The inclusion of the extra composite particles also modifies the oblique corrections of the SM, the values of which have been extracted from high precision experiments. Consequently, the validity of our model depends on the condition that the extra particles do not contradict those experimental results. These oblique corrections are parametrized in terms of the two well known quantities $T$ and $S$. The $T$ parameter is defined as [89,91–94]:

$$ T = \frac{\Pi_{33}(0) - \Pi_{11}(0)}{M_W^2 \alpha_{em}(m_Z)}. \quad (3.8) $$

where $\Pi_{11}(0)$ and $\Pi_{33}(0)$ are the vacuum polarization amplitudes at $q^2 = 0$ for loop diagrams having gauge bosons $W_\mu^3$, $W_\mu^1$, and $W_\mu^2$, in the external lines, respectively.

The one-loop diagrams that contribute to the $T$ parameter should include the hypercharge gauge boson $B_\mu^0$, since the $g'$ coupling is one of the sources of custodial symmetry breaking. The other source comes from the difference between up- and down-type quark Yukawa couplings.

In turn, the $S$ parameter is defined by [89,91–94]:

$$ S = \frac{4 \sin^2 \theta_W}{\alpha_{em}(m_Z)} \frac{d \Pi_{30}(q^2)}{dq^2} \bigg|_{q^2=0}. \quad (3.9) $$

where $\Pi_{30}(q^2)$ is the vacuum polarization amplitude for a loop diagram having $W_\mu^3$ and $B_\mu$ in the external lines.

The corresponding Feynman diagrams and details of the lengthy calculation of $T$ and $S$ that includes the extra particles in the loops are included in Appendix B.

Let us now address the masses of the composite scalars $h$, $H$, and $\eta$. In order to fit the particle spectrum observed so far, the model should contain one scalar with mass at 125.5 GeV, which we call $h$, while the heavier $H$ and $\eta$ should have masses satisfying the experimental bound $600 \text{ GeV} \lesssim m_H, m_\eta \lesssim 1 \text{ TeV}$. These masses have tree-level contributions directly from the scalar potential, but also important one-loop contributions from the Feynman diagrams shown in Appendix C. All these one-loop diagrams have quadratic and some have also quartic sensitivity to the ultraviolet cutoff $\Lambda$ of the effective theory. The calculation details are included in Appendix C. As shown there, the contact interaction diagrams involving $V_\mu$ and $A_\mu$ in the internal lines interfere destructively with those involving trilinear couplings between the heavy spin-0 and spin-1 bosons. As shown in Eqs. (2.26) and (2.27), the quartic couplings of a pair of spin-1 fields with two $h$’s are equal to those with two $H$’s. This implies that contact interactions contribute at one-loop level equally to the $h$ and $H$ masses. On the other hand, since the couplings of two spin-1 fields with one $h$ or one $H$ are different, i.e., $ahWW \neq aHWW, ahAA \neq aHAA, ahWA \neq aHWA, ahZA \neq aHZA$, these loop contributions cause the masses $m_h$ and $m_H$ to be significantly different, the former being much smaller than the latter (notice that in the Standard Model, $ahWW = b_{hWW} = 1$, implying an exact cancelation of the quartic divergences in the one-loop contributions to the Higgs mass). As it turns out, one can easily find conditions where the terms that are quartic in the cutoff cause partial cancelations in $m_h$, but not so in $m_H$ and $m_\eta$, making $m_h$ much lighter that the cutoff $\Lambda$ (e.g. $m_h \sim 126$ GeV) while $m_H$ and $m_\eta$ remain heavy (Fig. 2).

In Fig. 3a, b we show the sensitivity of the light scalar mass $m_h$ to variations of $M_V$ and $a_{hvt}$, respectively. These figures show that the values of $M_V$ and $a_{hvt}$ have an important effect on $m_h$. We can see that these models with composite vectors and axial vectors have the potential to generate scalar masses well below the supposed value around the cutoff, but only in a rather restricted range of parameters. The high sensitivity to the parameters, however, does not exhibit a fine tuning in the usual sense: that deviations from the adjusted point would always bring the mass back to a “naturally high” value near the cutoff. Here, the adjustment of parameters could bring the light scalar mass either back up or further below the actual value of 126 GeV.

### 4 Numerical study of the effects on $T$, $S$, and $h \rightarrow \gamma \gamma$

Let us first study the masses of $h$, $H$, and $\eta$ up to one loop. The one-loop diagrams are shown in Appendix C. In order to reduce the parameter space, we assume approximate universality in the quartic couplings of the scalar potential, i.e. $\kappa_1 = \kappa_2 = \kappa_3 = \lambda_1 = \lambda_3 = 1$, with the sole exception of $\lambda_2$ which is given by Eq. (A.12) in order that $h$, $H$, and $\eta$ become mass eigenstates (see Appendix A for details). As stated in the previous section, we define $h$ to be the recently
discovered Higgs boson of mass 125.5 GeV, while $H$ and $\eta$ should be heavier, their masses satisfying the experimental bound $600 \text{ GeV} \lesssim m_H, m_\eta \lesssim 1 \text{ TeV}$. The masses $m_h, m_H$, and $m_\eta$ depend on five free parameters: $a_{Htt}, a_{Htt}, a_{qtt}, M_V,$ and $\kappa = M_\eta^2/M_H^2$. We will constrain $a_{Htt}, M_V,$ and $\kappa$ by the following observables: the Higgs boson mass $m_h = 125.5$ GeV, the two-photon signal $0.78 \lesssim R_{\gamma\gamma} \lesssim 1.55$ (where we use 0.78 and 1.55, the central values of CMS and ATLAS recent results, respectively) and the oblique parameter $T$. On the other hand, $a_{Htt}, a_{qtt}$ will be more loosely constrained by the masses of $H$ and $\eta$. Finally, regarding the modified $W^3-B^0$ mixing coupling $c_{WB}$ [see Eq. (2.1)], it will be constrained by the $S$ parameter.

Let us now analyze in more detail the constraints imposed on our parameters by the values of $T$ and $S$ obtained from experimental high precision tests. The definitions of $T$ and $S$ and their calculation within our model are given in Appendix B [see Eqs. (B.1) and (B.30)]. As shown there, our expressions for $T$ and $S$ exhibit quartic, quadratic and logarithmic dependence on the cutoff $\Lambda \sim 3 \text{ TeV}$. However, the contributions from loops containing $h, H,$ and $\eta$ are not very sensitive to the cutoff, as they do not contain quartic terms in $\Lambda$. As a consequence, $T$ and $S$ happen to have a rather mild dependence on $m_H$ and $m_\eta$. In contrast, most of the other diagrams, i.e. those containing the spin-1 fields (SM gauge bosons and composite $V_\mu$ or $A_\mu$) have quartic dependence on the cutoff, and as a consequence they are very sensitive to the masses $M_V$ and $M_A$.

We can separate the contributions to $T$ and $S$ as $T = T_{SM} + \Delta T$ and $S = S_{SM} + \Delta S$, where

$$T_{SM} = -\frac{3}{16\pi \cos^2 \theta_W} \ln \left( \frac{m_h^2}{m_W^2} \right), \quad S_{SM} = \frac{1}{12\pi} \ln \left( \frac{m_h^2}{m_W^2} \right).$$

(4.1)

are the contributions within the SM, while $\Delta T$ and $\Delta S$ contain all the contributions involving the extra particles.

The experimental results on $T$ and $S$ restrict $\Delta T$ and $\Delta S$ to lie inside a region in the $\Delta S-\Delta T$ plane. At the 95 % CL (confident level), these regions are the elliptic contours shown in Fig. 4. The origin $\Delta S = \Delta T = 0$ corresponds to the Standard Model value, with $m_h = 125.5$ GeV and $m_t = 176$ GeV.

We can now study the restrictions on $a_{Htt}, M_V$, and $\kappa$ imposed by the value of the Higgs mass $m_h = 125.5$ GeV, by the $h \rightarrow \gamma\gamma$ signal within the range $0.78 \lesssim R_{\gamma\gamma} \lesssim 1.55$, and the previously described bounds imposed by the $T$ and $S$ parameters at 95 % CL.

After scanning the parameter space we find that the heavy vector mass has to be in the range $1.51 \text{ TeV} \lesssim M_V \lesssim 1.75$ TeV in order for the $T$ parameter to be within its bounds. Regarding the mass ratio $\kappa = M_\eta^2/M_H^2$ and the Higgs–top coupling $a_{Htt}$, we find that they have to be in the ranges $0.75 \lesssim \kappa \lesssim 0.78$ and $2.53 \lesssim a_{Htt} \lesssim 2.72$, respectively. Therefore, the Higgs boson, $h$, in this model couples strongly with the top quark, yet without spoiling the perturbative regime in the sense that the condition $a_{Htt}^2/4\pi \lesssim 1$ is still fulfilled.

Concerning the coupling of the top quark to the heavy pseudoscalar $\eta$, by imposing the experimental bound on heavy spin-0 particles $600 \text{ GeV} \lesssim m_\eta \lesssim 1$ TeV, we find that the coupling has the bound $a_{qtt} \lesssim 1.39$ for $M_V \simeq 1.51$ TeV, $\kappa \simeq 0.75$ (lower bounds), and $a_{qtt} \lesssim 1.46$ for $M_V \simeq 1.75$ TeV, $\kappa \simeq 0.78$ (upper bounds).

Regarding the coupling of the top quark to the heavy scalar $H$, we find that it grows with $m_H$ and, at the lower bound $m_H \sim 600$ GeV, it is restricted to be $a_{Htt} \simeq 3.53$, which implies that $H$ also couples strongly to the top quark. Lower values of the coupling $a_{Htt}$ will result if $H$ were lighter than 600 GeV, the experimental bound for heavy spin-0 particles.
Nevertheless, as before, this large coupling $a_{Htt}$ is still consistent with the perturbative regime as it satisfies $\frac{a_{Htt}}{\alpha} \lesssim 1$.

Besides jeopardizing the perturbative regime, these large couplings may cause violation of unitarity in longitudinal gauge boson scattering. Accordingly, we also checked that the aforementioned values of top quark couplings $a_{htt}, a_{Htt},$ and $a_{qtt}$ do not cause violation of the unitarity constraint for the scattering of gauge fields into fermion pairs for any energy up to $\sqrt{s} = \Lambda \simeq 3$ TeV.

Let us now study the restrictions imposed by the $h \to \gamma \gamma$ signal, expressed in Eq. (3.7). We explored the parameter space of $M_V$ and $\kappa$ ($\kappa = M_V^2/M_A^2$) trying to find values for $R_{\gamma\gamma}$ within a range more or less consistent with the ATLAS and CMS results. In Fig. 2 we show $R_{\gamma\gamma}$ as a function of $\kappa$, for the fixed values $g_C v = 0.8$ TeV and $a_{htt} = 2.6$. We chose $a_{htt} = 2.6$, which is near the center of the range $2.53 \lesssim a_{htt} \lesssim 2.72$ imposed by a light Higgs boson mass of $m_h = 125.5$ GeV, as previously described. In turn, the value $g_C v$ was chosen in order to fulfill the condition $\frac{g_C^2 v}{\Lambda^2} \lesssim 1$, which implies $g_C v \lesssim 0.9$ TeV. In any case, we checked that our prediction on $R_{\gamma\gamma}$ stays almost at the same value when the scale $g_C v$ is varied from 0.8 to 1 TeV. This occurs because the loop function $F_1(\beta)$ [see Eq. (3.4)] is rather insensitive to $\beta$ in the corresponding range.

Considering the bounds for $\kappa$ shown in Fig. 2, together with the restriction imposed by $T$ to be within its 95% CL, we found that $M_A$ should have a value in a rather narrow range $1.78$–$1.9$ TeV, while $M_V \lesssim 0.9M_A$. To arrive at this conclusion, we selected three representative values of the axial vector mass $M_A$, namely at $1.78, 1.8$, and $1.9$ TeV, and then we computed the resulting $T$ and $S$ parameters. We recall that SM point, which corresponds to $\Delta T = \Delta S = 0$ is included in the allowed parameter space identified in our analysis.

For each of these values of $M_A$, we found that the corresponding values of $M_V$ have to be in the ranges $1.54 \text{ TeV} \lesssim M_V \lesssim 1.57$ TeV, $1.56 \text{ TeV} \lesssim M_V \lesssim 1.59$ TeV and $1.65 \text{ TeV} \lesssim M_V \lesssim 1.68$ TeV in order to have $R_{\gamma\gamma}$ within the range $0.78 \lesssim R_{\gamma\gamma} \lesssim 1.55$ and the light Higgs to have a mass $m_h = 125.5$ GeV, without spoiling the condition $\frac{g_C^2 v}{\Lambda^2} \lesssim 1$.

Now, continuing with the analysis of the constraints in the $\Delta T$–$\Delta S$ plane, we also find that, in order to fulfill the constraint on $\Delta S$ as well, an additional condition must be met: for the aforementioned range of values of $M_V$ and $M_A$, the $S$ parameter turns out to be unacceptably large, unless a modified $W^3-B^0$ mixing is added. Here we introduce this mixing in terms of a coupling $c_{WB}$ [see Eq. (2.1)]. While $\Delta T$ does not depend much on this coupling, $\Delta S$ does depend on it, because this coupling enters in the quadratically divergent loop diagrams involving the $\pi^+\pi^-W^3B^0$ and $\pi^0\pi^2W^3B^0$ contact interactions (where $\pi^i$ are the SM Goldstone bosons), as well as in the $W^3-B^0$ tree-level mixing diagram.

In Fig. 4a–c we show the allowed regions for the $\Delta T$ and $\Delta S$ parameters, for the three sets of values of $M_V$ and $M_A$ previously indicated. The ellipses denote the experimentally allowed region at 95% CL, while the horizontal line shows the values of $\Delta T$ and $\Delta S$ in the model, as the mixing parameter $c_{WB}$ is varied over the specified range in each case. The lines are horizontal because $\Delta T$ does not depend on $c_{WB}$. As seen in the figures, $c_{WB}$ must be in the

---

**Fig. 4** The $\Delta S$–$\Delta T$ plane in our model with composite scalars and vector fields. The ellipses denote the experimentally allowed region at 95% CL taken from [109]. The origin $\Delta S = \Delta T = 0$ corresponds to the Standard Model value, with $m_h = 125.5$ GeV and $m_t = 176$ GeV. a–c Correspond to three different sets of values for the masses $M_V$ and $M_A$, as indicated. The horizontal line shows the values of $\Delta S$ and $\Delta T$ in the model, as the mixing parameter $c_{WB}$ varies over the ranges $0.228 \leq c_{WB} \leq 0.231$ (a), $0.208 \leq c_{WB} \leq 0.212$ (b), and $0.180 \leq c_{WB} \leq 0.182$ (c).
ranges $0.228 \leq c_{WB} \leq 0.231$, $0.208 \leq c_{WB} \leq 0.212$ and $0.180 \leq c_{WB} \leq 0.182$ for the cases $M_A = 1.78$, 1.8 and 1.9 TeV, respectively. Notice that the case $c_{WB} = 0$ is clearly excluded, as $\Delta S$ would be smaller than its lower bound (the point would be further to the left of the corresponding ellipse).

As a final remark, we should notice that the model of Ref. [110] is different from ours in the sense that they use a tensor formulation instead of a vector formulation to describe the heavy spin-1 fields, their spectrum does not include a pseudoscalar and, more important, the interactions involving more than one heavy spin-1 field are not considered, so that vertices like $hVV$ and $hAA$ are absent. This implies that the heavy spin-1 particles do not play a role in the $h \rightarrow \gamma\gamma$ decay. However, that model does consider an interaction between the scalar, the SM gauge bosons and the axial vector involving a covariant derivative of the scalar field, which we do not consider in the present work.

5 Conclusions

We studied a framework of electroweak symmetry breaking without fundamental scalars, based on an underlying dynamics that becomes strong at a scale which we assume $\Lambda = 4\pi v - 3$ TeV. In general, below this scale there could be composite states bound by the strong dynamics. The spectrum of composite fields with masses below $\Lambda$ was assumed to consist of spin-0 and spin-1 fields only, and the interactions among these particles and those of the Standard Model was described by means of a $SU(2)_L \times SU(2)_R / SU(2)_{L+R}$ effective chiral Lagrangian. Specifically, the composite fields included here were two scalars, $h$ and $H$, one pseudoscalar $\eta$, a vector triplet $V^\mu_\nu$, and an axial-vector triplet $A^\mu_\nu$. The lightest scalar, $h$, was taken to be the newly discovered state at the LHC, with mass $\sim 125.5$ GeV. In this scenario, in general one must include a deviation of the Higgs–fermion couplings with respect to the SM, which we denote here as $a_{fff}$. In particular, the coupling of the light Higgs to the top quark, $a_{htt}$, is constrained from the requirement of having $m_h \simeq 125.5$ GeV and a $h \rightarrow \gamma\gamma$ signal in the range $0.78 \lesssim R_{\gamma\gamma} \lesssim 1.55$ (where we use 0.78 and 1.55, the central values of CMS and ATLAS recent results, respectively).

Our main goal within this framework was to study the consistency of having this spectrum of composite particles, regarding the loop processes that these extra particles may affect, specifically the rate $h \rightarrow \gamma\gamma$, which is a crucial signal for the Higgs, and the high precision electroweak parameters $T$ and $S$.

Besides requiring that the scalar spectrum in our model includes a 125.5 GeV Higgs boson, the other two spin-0 states, namely $H$ and $\eta$, must be heavier and within the experimental bounds $600$ GeV $\lesssim m_H, m_\eta \lesssim 1$ TeV.

We found that the known value of the $T$ parameter at the 95% CL, together with the observed $h \rightarrow \gamma\gamma$ rate, restrict the mass of the axial vector to be in the range $1.8$ TeV $\lesssim m_A \lesssim 1.9$ TeV and imply that the mass ratio $\kappa = M_V^2 / M_A^2$ should satisfy the bound $0.75 \lesssim \kappa \lesssim 0.78$.

In addition, consistency with the experimental value on the $S$ parameter required the presence of a modified $W^3 - B^0$ mixing, which we parametrized in terms of a coupling $c_{WB}$. We found that a non-zero value for this coupling was necessary. The precise value depends on the masses $M_V$ and $M_A$, but within the ranges quoted above, $c_{WB}$ is about 0.2.

We also found that the $T$ and $S$ parameters have low sensitivity to the masses of the scalar and pseudoscalar composites, because the dominant contributions to $T$ and $S$ arise from quartic divergent terms, which only depend on the heavy vector and axial-vector masses, not on the scalars. Consequently, from the point of view of the $T$ and $S$ values, the masses of the heavy scalars and pseudoscalars are not restricted.

Furthermore, we have found that one-loop effects are crucial to account for the mass hierarchy between the 125.5 GeV Higgs boson, $h$, and the heavier states $H$ and $\eta$.

The requirement of having a light 125.5 GeV Higgs boson without spoiling the $T$ parameter and the $h \rightarrow \gamma\gamma$ constraints implies that this Higgs boson must couple strongly to the top quark by a factor of about 2 larger than the Standard Model case. More precisely, the bound $0.78 \lesssim R_{\gamma\gamma} \lesssim 1.55$ constrains the $h$ to top quark coupling to be in the range $2.53 \lesssim a_{htt} \lesssim 2.72$. Regarding the heavy scalar $H$, we find that it should have a mass close to its lower bound of 600 GeV for a $H$ to top quark coupling as low as $a_{Htt} \sim 3.5$. This value implies that $H$ also couples strongly to the top quark. Lower values of $a_{Htt}$ will result in an $H$ lighter than the 600 GeV experimental lower bound. On the other hand, we found that the value of the $\eta$ to top quark coupling $a_{\eta tt}$ can vary from 0 to about 1.5.

In summary, we find that composite vectors and axial vectors do have an important effect on the rate $h \rightarrow \gamma\gamma$, and on the $T$ and $S$ parameters, and that one can find values for their masses that are consistent with the experimental values on the previous parameters. However, one does require an extra $W^3 - B^0$ mixing, which in any case can be included in the Lagrangian still respecting all the symmetries. We also find that modified top quark to scalar and to pseudoscalar couplings may appear, in order to have a spectrum with a light 125.5 GeV Higgs boson, and with heavier scalar and pseudoscalar states consistent with the experimental allowed range $600$ GeV $\lesssim m_H, m_\eta \lesssim 1$ TeV.

Note that we find quartic and quadratic divergences in both $T$ and $S$, while deconstructed models only yield logarithmic divergences for both parameters. This is due to the kinetic mixings between the SM gauge bosons and the...
heavy spin-1 fields, which modify their propagators, introducing different loop contributions to the oblique parameters. Also worth mentioning is that we did not include composite fermions below the cutoff scale $\Lambda \sim 3$ TeV, which may affect the oblique $T$ and $S$ parameters as well. An extension of the model could include composite quarks, a fourth quark generation and/or vector-like quarks. Their effects on the oblique parameters and on the $h \to \gamma \gamma$ decay rate may be worth studying. Since the inclusion of extra quarks gives a positive contribution to the $T$ parameter as shown in Refs. [24, 26, 38, 81], we expect that an extension of the quark sector will increase the upper bound on the axial-vector mass obtained from oblique parameter constraints, because the $T$ parameter takes negative values when the heavy axial-vector mass is increased. Addressing all these issues requires an additional and careful analysis that we have left outside the scope of this work.

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Appendix A: Spontaneously broken gauge theory based on $SU(2)_L \times SU(2)_C \times SU(2)_D \times U(1)_Y$

Let us consider a theory with a gauge group of 4 sites, $SU(2)_L \times SU(2)_C \times SU(2)_D \times U(1)_Y$. We will assume that the interactions at some energy scale above a few TeV will cause the condensation of fermion bilinears, in a way somewhat analogous to what happens in QCD at the chiral symmetry breaking scale. The gauge symmetry is thus spontaneously broken to $U(1)_{em}$. The dynamical fields that are left below the symmetry breaking scale will obey an effective non-linear sigma model Lagrangian of the form

$$\mathcal{L} = \mathcal{L}_{\text{gauge}} + \mathcal{L}_{\chi} - V(\Sigma_{LC}, \Sigma_{CD}, \Sigma_{DY}), \quad (A.1)$$

where $\mathcal{L}_{\text{gauge}}$ is the Lagrangian of the gauge fields, $\mathcal{L}_{\chi}$ contains the kinetic terms for the Higgs fields that will break the gauge symmetry when the Higgses acquire vacuum expectation values, and $V(\Sigma_{LC}, \Sigma_{CD}, \Sigma_{DY})$ is the Higgs interaction potential. They are given by

$$\mathcal{L}_{\text{gauge}} = - \sum_I \frac{1}{2g_I^2} \left\{ \omega_{\mu\nu}^I \omega_{\mu\nu}^I \right\}, \quad \text{with } I = L, C, D, Y, \quad (A.2)$$

$$\mathcal{L}_{\chi} = 2v_{LC}^2 \left( D_\mu \Sigma_{LC} D^\mu \Sigma_{LC}^+ \right) + 2v_{CD}^2 \left( D_\mu \Sigma_{CD} D^\mu \Sigma_{CD}^+ \right) + 2v_{DY}^2 \left( D_\mu \Sigma_{DY} D^\mu \Sigma_{DY}^+ \right), \quad (A.3)$$

and

$$V(\Sigma_{LC}, \Sigma_{CD}, \Sigma_{DY}) = - \frac{\mu_{LC}^2 v_{LC}^2}{2} \left( \Sigma_{LC} \Sigma_{LC}^+ \right) - \frac{\mu_{CD}^2 v_{CD}^2}{2} \left( \Sigma_{CD} \Sigma_{CD}^+ \right) - \frac{\mu_{DY}^2 v_{DY}^2}{2} \left( \Sigma_{DY} \Sigma_{DY}^+ \right) + \frac{\lambda_1 v_{LC}^4}{4} \left( \left( \Sigma_{LC} \Sigma_{LC}^+ \right) \right)^2 + \frac{\lambda_2 v_{CD}^4}{4} \left( \left( \Sigma_{CD} \Sigma_{CD}^+ \right) \right)^2 + \frac{\lambda_3 v_{DY}^4}{4} \left( \left( \Sigma_{DY} \Sigma_{DY}^+ \right) \right)^2 + \kappa_1 v_{CD}^2 v_{LC}^2 \times \left( \Sigma_{CD} \Sigma_{LC}^+ \right) + \kappa_2 v_{CD}^2 v_{DY}^2 \times \left( \Sigma_{DY} \Sigma_{CD}^+ \right) + \kappa_3 v_{CD}^2 v_{DY}^2 \times \left( \Sigma_{DY} \Sigma_{CD}^+ \right). \quad (A.4)$$

The covariant derivates are defined as

$$D_\mu \Sigma_{IJ} = \partial_\mu \Sigma_{IJ} - i \omega_{\mu}^I \Sigma_{IJ} + i \Sigma_{IJ} \omega_{\mu}^I, \quad (A.5)$$

where $\omega_{\mu}^I = (W_\mu, \bar{\nu}_\mu, \bar{\alpha}_\mu, B_\mu)$ with

$$B_\mu = \frac{g'}{2} B_\mu^a \tau^a, \quad W_\mu = \frac{g}{2} W_\mu^a \tau^a. \quad (A.6)$$

$$v_\mu = \frac{gC}{2} v_\mu^a \tau^a, \quad a_\mu = \frac{gC}{2} a_\mu^a \tau^a, \quad (A.7)$$

where it has been assumed that $gC = g_D$ and the indices $I, J$ stand for $I, J = L, C, D, Y$. In turn, the field strength tensors are generically given by

$$\omega_{\mu\nu}^I = \partial_\mu \omega_{\nu}^I - \partial_\nu \omega_{\mu}^I - i \left[ \omega_{\mu}^I, \omega_{\nu}^I \right]. \quad (A.8)$$
To ensure the correct normalization for the Goldstone bosons kinetic terms, $\Sigma_{LC}$, $\Sigma_{DY}$, and $\Sigma_{CD}$ are defined as

$$\Sigma_{LC} = \left(1 + \frac{\eta - \frac{1}{\sqrt{2}} h + \frac{1}{\sqrt{2}} H}{4v_{LC}} \right) U_{LC},$$

with $U_{LC} = \exp \left[ i \frac{\eta - \frac{1}{\sqrt{2}} h + \frac{1}{\sqrt{2}} \rho}{4v_{LC}} \right]$, \hspace{1cm} (A.9)

$$\Sigma_{DY} = \left(1 + \frac{-\eta - \frac{1}{\sqrt{2}} h + \frac{1}{\sqrt{2}} H}{4v_{DY}} \right) U_{DY},$$

with $U_{DY} = \exp \left[ i \frac{-\pi - \frac{1}{\sqrt{2}} \sigma + \frac{1}{\sqrt{2}} \rho}{4v_{DY}} \right]$, \hspace{1cm} (A.10)

$$\Sigma_{CD} = \left(1 + \frac{h + H}{4v_{CD}} \right) U_{CD},$$

with $U_{CD} = \exp \left[ i \frac{\sigma + \rho}{4v_{CD}} \right]$,

$$v_{LC} = v_{DY},$$ \hspace{1cm} (A.11)

where $\pi = \pi^a \tau^a$, $\sigma = \sigma^a \tau^a$ and $\rho = \rho^a \tau^a$ the Goldstone bosons associated with the SM gauge bosons, the heavy vectors and heavy axial vectors, respectively, and $\tau^a$ the usual Pauli matrices. In turn, $h$ and $H$ are the massive scalars and $\eta$ is the massive pseudoscalar.

It is worth mentioning that $h$, $H$, and $\eta$ are physical scalar fields when the following relations are fulfilled:

$$\lambda_1 = \lambda_3, \quad \kappa_1 = \kappa_3, \quad \lambda_2 = \sqrt{2\kappa_2 + \lambda_3^2} \frac{v_{LC}}{v_{CD}}.$$ \hspace{1cm} (A.12)

The three Higgs doublets acquire vacuum expectation values, thus causing the spontaneous breaking of the $SU(2)_L \times SU(2)_C \times SU(2)_D \times U(1)_Y$ local symmetry down to $U(1)_{em}$, while the global group $G = SU(2)_L \times SU(2)_C \times SU(2)_D \times SU(2)_R$ is broken to the diagonal subgroup $H = SU(2)_L \times SU(2)_R$. The Goldstone boson fields $U_{IJ}$ can be put in the form

$$U_{IJ} = \xi_I \xi_J^\dagger, \quad \text{where} \quad U_{IJ} \in \frac{SU(2)_I \times SU(2)_J}{H},$$

$$I, J = L, C, D, Y.$$ \hspace{1cm} (A.13)

These $\xi_I$ transform under the full $SU(2)_L \times SU(2)_C \times SU(2)_D \times U(1)_Y$ as $\xi_I \rightarrow g_I \xi_I^\dagger$. Choosing a gauge transformation $g_I = \xi_I^\dagger$ we can transfer the would-be Goldstone bosons to degrees of freedom of the gauge fields:

$$U_{IJ} \rightarrow \xi_I^\dagger U_{IJ} \xi_J = 1, \quad \omega_{\mu I} \rightarrow \xi_I^\dagger \omega_{\mu I}^I \xi_I + i \xi_I^\dagger \partial_\mu \xi_I = \Omega_{\mu}^I,$$ \hspace{1cm} (A.14)

and the Lagrangian of Eq. (A.3) reduces to

$$L_{\text{gauge}}^\mu = 2v_{LC}^2 \left(1 + \frac{\eta - \frac{1}{\sqrt{2}} h + \frac{1}{\sqrt{2}} H}{4v_{LC}} \right)^2 \left(\Omega_{\mu}^I - \Omega_\mu^I\right)^2,\hspace{1cm} (A.14)$$

$$+ 2v_{LC}^2 \left(1 + \frac{-\eta - \frac{1}{\sqrt{2}} h + \frac{1}{\sqrt{2}} H}{4v_{LC}} \right)^2 \left(\Omega_\mu^I - \Omega_\mu^I\right)^2,$$

$$\times \left(\Omega_\mu^I - \Omega_\mu^I\right)^2,\hspace{1cm} (A.15)$$

Specifically, we will do a partial gauge fixing resulting in $\xi_Y = \xi_L^I = e^{i \pi / 4 v_{LC}} \xi_I$ and $\xi_C = \xi_D = 1$, which implies that $\sigma = \rho = 0$ and $U_{DY} = U_{CL}$. This gauge fixing corresponds to the unitary gauge where the Goldstone boson triplets $\sigma$ and $\rho$ are absorbed as longitudinal modes of $\Omega_C^I$ and $\Omega_D^I$. These fields now transform under $SU(2)_L \times SU(2)_R$ according to

$$\Omega_{\mu}^C \rightarrow h \Omega_{\mu}^C h^\dagger + i h \partial_\mu h^\dagger.$$ \hspace{1cm} (A.16)

The $\Omega_C^I$ and $\Omega_D^I$ can be decomposed with respect to parity as

$\Omega_{\mu}^C = v_\mu + a_\mu, \quad \Omega_{\mu}^D = v_\mu - a_\mu,$ \hspace{1cm} (A.17)

so that under $SU(2)_L \times SU(2)_R$ one has the following transformations:

$$v_\mu \rightarrow h v_\mu h^\dagger + i h \partial_\mu h^\dagger, \quad a_\mu \rightarrow h a_\mu h^\dagger.$$ \hspace{1cm} (A.18)

Defining

$$v_{\mu \nu} = \partial_\mu v_\nu - \partial_\nu v_\mu - i [v_\mu, v_\nu] \quad \text{and} \quad D_{\mu}^V a_\nu = \partial_\mu a_\nu - i [v_\mu, a_\nu]$$ \hspace{1cm} (A.19)

we can write the interactions of the gauge sector of Eq. (A.2) in the form [54,56]:

$$L_{\text{gauge}} = L_{\text{gauge, SM}} - \frac{1}{2g_C^2} \left( (v_{\mu \nu} - i [a_\mu, a_\nu])^2 \right),$$

$$- \frac{1}{2g_C^2} \left( D_{\mu}^V a_\nu - D_{\nu}^V a_\mu \right)^2.$$ \hspace{1cm} (A.20)

Now, due to mixing with the SM fields, $v_\mu$ and $a_\mu$ are not mass eigenstates. The vector and axial-vector mass eigenstates as $V_\mu$ and $A_\mu$, respectively, are actually given by the following relations [54,56]:

$$\xi_T = \xi_L^I = e^{i \pi / 4 v_{LC}} \xi_I + i \xi_T^\dagger \partial_\mu \xi_T = \Omega_T^I.$$ \hspace{1cm} (A.21)
\[ V_\mu = v_\mu - i \Gamma_\mu, \quad A_\mu = a_\mu + \frac{\kappa}{2} u_\mu, \quad (A.21) \]

where \( \kappa \) will be determined below, and \( \Gamma_\mu \) is defined as

\[ \Gamma_\mu \equiv \frac{1}{2i} \left( \Omega^Y_\mu + \Omega^L_\mu \right) \quad (A.22) \]

\[ = \frac{1}{2} \left[ u^\dagger (\partial_\mu - i B_\mu) u + u (\partial_\mu - i W_\mu) u^\dagger \right]. \]

Considering these definitions, the strength tensors satisfy the following identities:

\[ v_{\mu\nu} = V_{\mu\nu} - i \left[ V_\mu, V_\nu \right] + \frac{i}{4} \left[ u_\mu, u_\nu \right] + \frac{1}{2} \left( u W_\mu u^\dagger \right), \quad (A.23) \]

\[ a_{\mu\nu} = A_{\mu\nu} - \frac{\kappa}{2} u_{\mu\nu} - i \left[ V_\mu, A_\nu - \frac{\kappa}{2} u_\nu \right] + i \left[ V_\nu, A_\mu - \frac{\kappa}{2} u_\mu \right], \quad (A.24) \]

where

\[ W_\mu = \partial_\mu W_\nu - \partial_\nu W_\mu - i \left[ W_\mu, W_\nu \right], \quad B_\mu = \partial_\mu B_\nu - \partial_\nu B_\mu. \]

\[ V_{\mu\nu} = \nabla_\mu V_\nu - \nabla_\nu V_\mu = \partial_\mu V_\nu - \partial_\nu V_\mu + \left[ \Gamma_\mu, V_\nu \right] - \left[ \Gamma_\nu, V_\mu \right], \quad (A.25) \]

\[ A_{\mu\nu} = \nabla_\mu A_\nu - \nabla_\nu A_\mu = \partial_\mu A_\nu - \partial_\nu A_\mu + \left[ \Gamma_\mu, A_\nu \right] - \left[ \Gamma_\nu, A_\mu \right], \quad (A.26) \]

\[ u_{\mu\nu} = \partial_\mu u_\nu - \partial_\nu u_\mu + \left[ \Gamma_\mu, u_\nu \right] - \left[ \Gamma_\nu, u_\mu \right]. \quad (A.27) \]

With these definitions and the aforementioned gauge fixing, the symmetry breaking sector of the Lagrangian becomes

\[ \mathcal{L}^{gauge}_K = 4v^2_{LC} \left( 1 + \frac{H - h}{2\sqrt{2}v_{LC}} + \frac{(H - h)^2}{32v^2_{LC}} + \frac{\eta^2}{16v^2_{LC}} \right) \]

\[ \times \left[ \left\langle V_\mu V^\mu \right\rangle + \left\langle A_\mu A^\mu \right\rangle \right] \]

\[ + \left( \frac{1 - \kappa}{2} \right)^2 \left\langle u_\mu u^\mu \right\rangle + \left( 1 - \kappa \right) \left\langle A_\mu u^\mu \right\rangle \]

\[ + 4v_{LC} \eta \left( 1 + \frac{H - h}{4v_{LC}} \right) \]

\[ \times \left[ \left\langle V_\mu A^\mu \right\rangle + \frac{1 - \kappa}{2} \left\langle V_\mu u^\mu \right\rangle \right] \]

\[ + 8v^2_{CD} \left( 1 + \frac{H - h}{2v_{CD}} + \frac{h^2 + 2hh + H^2}{16v^2_{CD}} \right) \]

\[ \times \left[ \left\langle A_\mu A^\mu \right\rangle + \frac{\kappa^2}{4} \left\langle u_\mu u^\mu \right\rangle - \kappa \left\langle A_\mu u^\mu \right\rangle \right] \]

\[ + \frac{1}{2} \partial_\mu \eta \partial^\mu \eta + \frac{1}{2} \partial_\mu h \partial^\mu h + \frac{1}{2} \partial_\mu H \partial^\mu H, \quad (A.29) \]

where one defines

\[ u_\mu \equiv \Omega^Y_\mu - \Omega^L_\mu = iu^\dagger D_\mu U u^\dagger, \quad \text{with} \quad U = u^2 = e^{\frac{\pi}{2} a^\mu a^\mu}, \quad (A.30) \]

and

\[ D_\mu U = \partial_\mu U - i B_\mu U + i U W_\mu, \quad (A.31) \]

and where \( D_\mu \) is a covariant derivative containing the SM gauge fields only.

With the further replacement \( V_\mu \to \frac{g_C}{\sqrt{2}} V_\mu, A_\mu \to \frac{g_C}{\sqrt{2}} A_\mu \), the gauge sector of the Lagrangian becomes

\[ \mathcal{L}^{gauge}_{\text{gauge,SM}} = -\frac{1}{4} \left\langle V_\mu V^\mu \right\rangle - \frac{1}{4} \left\langle A_\mu A^\mu \right\rangle \]

\[ - \frac{i}{8g^2} \left( \left[ u_\mu, u^\mu \right] \left( u W_\mu u^\dagger + u^\dagger B_\mu u \right) \right) \]

\[ - \frac{\kappa^2}{8g^2} \left( \left[ u_\mu, u^\mu \right] \right) + \frac{1 - \kappa^2}{4g^2} \left( \left[ u_\mu, u^\mu \right] \right)^2 \]

\[ - \frac{1}{2} \sqrt{2} g^2 \left( \left[ u W_\mu u^\dagger + u^\dagger B_\mu u \right] \right) \]

\[ + \frac{\kappa}{2} \sqrt{2} g^2 \left( \left[ u_\mu, u^\mu \right] \right) \]

\[ + \frac{i}{2} \sqrt{2} g^2 \left( \left[ V_\mu, V^\mu \right] \right) \]

\[ - \frac{1 - \kappa^2}{4g^2} \left( \left[ u_\mu, u^\mu \right] \right) \]

\[ - \frac{\kappa}{8} \left( \left[ A_\mu, A^\mu \right] \right) \]

\[ + \frac{i}{4} \left( \left[ V_\mu, V^\mu \right] \right) \left( u W_\mu u^\dagger + u^\dagger B_\mu u \right) \]

\[ + \frac{i}{4} \left( \left[ A_\mu, A^\mu \right] \right) \left( u W_\mu u^\dagger + u^\dagger B_\mu u \right) \]

\[ + \frac{i g_C}{2} \left( \left[ V_\mu, V^\mu \right] \right) + \frac{i g_C}{2} \left( \left[ V_\mu, A^\mu \right] \right) \]

\[ + \frac{i g_C}{2} \left( \left[ A_\mu, A^\mu \right] \right) - \frac{\kappa g_C}{2} \left( \left[ A_\mu, A^\mu \right] \right) \]

\[ + \frac{\kappa g_C}{2} \left( \left[ V_\mu, A^\mu \right] \right) - \left( \left[ V_\mu, A^\mu \right] \right) \]

\[ + \frac{g^2}{4} \left( \left[ V_\mu, V^\mu \right] \right) + \frac{g^2}{4} \left( \left[ V_\mu, V^\mu \right] \right) \]
where the correct normalization of the kinetic terms of the heavy spin-1 resonances implies \([54,56]\):

\[
V_\mu = \frac{1}{\sqrt{2}} \tau^a V_{\mu}^a, \quad A_\mu = \frac{1}{\sqrt{2}} \tau^a A_{\mu}^a,
\]

(A.33)

while the symmetry breaking sector of the Lagrangian takes the following form:

\[
L^\text{gauge}_K = 4v_{\text{LC}}^2 \left( 1 + \frac{H - h}{2\sqrt{2}v_{\text{LC}}} + \frac{(H - h)^2}{32v_{\text{LC}}^2} + \frac{\eta^2}{16v_{\text{LC}}^2} \right)
\times \left[ \frac{g_C^2}{2} \langle V_\mu V^\mu \rangle + \frac{g_C^2}{2} \langle A_\mu A^\mu \rangle 
\right.
\]

\[
+ \left( 1 - \frac{\kappa}{2} \right) \eta \left( 1 + \frac{H - h}{4\sqrt{2}v_{\text{LC}}} \right)
\times \left[ \frac{g_C^2}{2} \langle V_\mu A^\mu \rangle + \frac{g_C}{\sqrt{2}} \left( 1 - \frac{\kappa}{2} \right) \langle V_\mu u^\mu \rangle \right]
\]

\[
+ 4v_{\text{LC}}^2 \eta^2 \left( 1 + \frac{H - h}{4\sqrt{2}v_{\text{LC}}} \right)
\times \left[ \frac{g_C^2}{2} \langle V_\mu A^\mu \rangle + \frac{g_C}{\sqrt{2}} \left( 1 - \frac{\kappa}{2} \right) \langle V_\mu u^\mu \rangle \right]
\]

\[
+ 8v_{\text{CD}}^2 \left( 1 + \frac{h + H}{2v_{\text{CD}}} + \frac{h^2 + 2hH + H^2}{16v_{\text{CD}}^2} \right)
\times \left[ \frac{g_C^2}{2} \langle A_\mu A^\mu \rangle + \frac{\kappa^2}{4} \langle u_\mu u^\mu \rangle - \frac{g_C}{\sqrt{2}} \langle A_\mu u^\mu \rangle \right]
\]

\[
+ \frac{1}{2} \partial_\mu h \partial^\mu h + \frac{1}{2} \partial_\mu H \partial^\mu H + \frac{1}{2} \partial_\mu \eta \partial^\mu \eta.
\]

(A.34)

Then from the expressions (A.34) and (A.37) it follows that the masses of \(V_{\mu}^a\) and \(A_{\mu}^a\) are determined by the parameters \(g_C\) and \(\kappa\) as

\[
M_V = \frac{g_C v}{\sqrt{1 - \kappa}}, \quad M_A = \frac{M_V}{\sqrt{\kappa}}.
\]

(A.38)

We now see that the diagonalization procedure determines \(\kappa\) in Eq. (A.21) as the mass ratio \(\kappa = M_V^2/M_A^2\). On the other hand, the strength of the gauge coupling \(g_C\) determines the absolute value of these masses. The coupling \(g_C\) also controls the kinetic mixing between \(V_{\mu}^a\) and the SM gauge bosons, while the kinetic mixing between \(A_{\mu}^a\) and the SM gauge bosons is controlled by both \(\kappa\) and \(g_C\), as seen in Eq. (A.32).

Consequently the Lagrangian that describes the interactions among the composite spin zero fields, the composite spin one fields and the SM gauge bosons and SM Goldstone bosons is given by

\[
L = L^\text{gauge} + L^\text{gauge}_K - V (\Sigma_{LC}, \Sigma_{CD}, \Sigma_{DY}).
\]

(A.39)

This same Lagrangian is described in Eq. (2.33), where the scalar potential has been expanded to quadratic factors of the scalar fields. We did not include the cubic and quartic scalar interactions in Eq. (2.33) as they are irrelevant to our calculations of the \(h \rightarrow \gamma \gamma\) decay rate and the oblique \(T\) and \(S\) parameters.

**Appendix B: Calculation of the \(T\) and \(S\) parameters**

The \(T\) parameter is defined as \([89,91–94]\):

\[
T = \frac{\tilde{T}}{a_{em} (m_Z^2)} = \frac{\Pi_{33} (0) - \Pi_{11} (0)}{M_W^2},
\]

(B.1)

where \(\Pi_{11} (0)\) and \(\Pi_{33} (0)\) are the vacuum polarization amplitudes for loop diagrams having gauge bosons \(W^1_\mu, W^2_\mu\) and \(W^3, W^3\) in the external lines, respectively. These vacuum polarization amplitudes are evaluated at \(q^2 = 0\), where \(q\) is the external momentum.

The one-loop diagrams that give contributions to the \(T\) parameter should include the hypercharge gauge boson \(B^0_\mu\) since the \(g'\) coupling is one of the sources of the breaking of the custodial symmetry. The other source of custodial symmetry breaking comes from the difference between up- and down-type quark Yukawa couplings. The corresponding Feynman diagrams are shown in Fig. 5 and we computed them in the Landau gauge for the SM gauge bosons and Goldstone bosons, where the global \(SU(2)_L \times U(1)_Y\) symmetry is preserved. Regarding the heavy composite spin-1 resonances, we use the unitary gauge for their propagators.
since the Lagrangian given in Eq. (2.33) does not include the Goldstone bosons associated to the longitudinal components of these heavy parity even and parity odd spin-1 resonances. From the Feynman diagrams shown in Fig. 5, it follows that the $\hat{T}$ parameter is given by

$$
\hat{T} = \hat{T}(\pi^2 B^0) + \hat{T}(V^3 B^0, \pi^2) + \hat{T}(V^3 B^0 V^3, \pi^2) + \hat{T}(V^2 B^0)
+ \hat{T}(\pi^2 B^0) + \hat{T}(V^3 B^0, V^2) + \hat{T}(A^2 B^0, A^2)
+ \hat{T}(V^3 B^0 V^3, V^2) + \hat{T}(A^2 B^0, A^2) + \hat{T}(V^3 B^0, A^2)
+ \hat{T}(A^3 B^0, V^2) + \hat{T}(V^3 B^0 V^3, A^2) + \hat{T}(A^3 B^0, A^2)
+ \hat{T}(V^3 B^0, A^3) + \hat{T}(V^3 B^0 A^3) + \hat{T}(V^3 B^0, V^3)
+ \hat{T}(A^3 B^0 A^3) + \hat{T}(V^3 B^0 A^3) + \hat{T}(V^3 B^0, V^3)
+ \hat{T}(A^3 B^0 A^3) + \hat{T}(V^3 B^0 A^3) + \hat{T}(V^3 B^0, V^3)
+ \hat{T}(A^3 B^0 A^3) + \hat{T}(V^3 B^0 A^3) + \hat{T}(V^3 B^0, V^3)
+ \hat{T}(A^3 B^0 A^3) + \hat{T}(V^3 B^0 A^3) + \hat{T}(V^3 B^0, V^3),
$$

(B.2)
where the different one-loop contributions to the $\hat{T}$ parameter are

\[
\hat{T}_{(\pi^2 B^0)} \simeq -\frac{3\alpha_{em}}{16\pi^2 \cos^2 \theta_W} \ln \left( \frac{\Lambda^2}{M_W^2} \right) - \frac{3\alpha_{em}}{32\pi^2 v^2 \cos^2 \theta_W} \left( f_v g V - \frac{1}{2} f_V^2 \right) \Lambda^2 + \frac{3\alpha_{em}}{8\pi^2 v^2 \cos^2 \theta_W} \Lambda^2, \tag{B.3}
\]

\[
\hat{T}_{(V^3 B^0,\pi^2)} \simeq -\frac{3\alpha_{em}}{16\pi^2 v^2 \cos^2 \theta_W} \left( f_v g V - \frac{1}{2} f_V^2 \right) \Lambda^4 - \frac{3\alpha_{em}}{8\pi^2 v^2 \cos^2 \theta_W} \left[ 1 - \left( f_v g V - \frac{1}{2} f_V^2 \right) \frac{M_V^2}{v^2} \right] \Lambda^4 - 6M_V^4 \left( M^2 - M_V^2 \right) \Lambda^4, \tag{B.4}
\]

\[
\hat{T}_{(V^3 B^0, \gamma^2)} \simeq -\frac{3\alpha_{em}}{128\pi^2 v^2 M^2 v^2 \cos^2 \theta_W} \left( f_v g V - 2g_v \right)^2 \Lambda^4 - 4M^2 \Lambda^2 + 6M_V^4 \left( M^2 - M_V^2 \right) \Lambda^4, \tag{B.5}
\]

\[
\hat{T}_{(V^2 B^0)} \simeq \frac{3\alpha_{em}}{128\pi^2 v^2 M^2 v^2 \cos^2 \theta_W} \Lambda^4 + \frac{3\alpha_{em}}{64\pi^2 v^2 \cos^2 \theta_W} \left( f_v g V - 2g_v \right)^2 \Lambda^4 - \frac{3\alpha_{em}}{64\pi^2 v^2 \cos^2 \theta_W} \Lambda^2 - M_V^2 \ln \left( \frac{\Lambda^2 + M_V^2}{M_V^2} \right), \tag{B.6}
\]

\[
\hat{T}_{(A^2 B^0)} \simeq -\frac{3\alpha_{em}}{128\pi^2 v^2 M^2 v^2 \cos^2 \theta_W} \Lambda^4 + \frac{3\alpha_{em}}{64\pi^2 v^2 \cos^2 \theta_W} \Lambda^2 - M_V^2 \ln \left( \frac{\Lambda^2 + M_V^2}{M_V^2} \right), \tag{B.7}
\]

\[
\hat{T}_{(V^3 B^0, \gamma^2)} \simeq -\frac{3\alpha_{em}}{64\pi^2 v^2 M^2 v^2 \cos^2 \theta_W} \left( f_v g V - 2g_v \right)^4 \Lambda^4 - 2 \left( f_v g V - 2g_v \right) M_V^2 \Lambda^2 - \frac{4}{M^2 - M_V^2} \left( f_v g V - 2g_v \right) M_V^4 \ln \left( \frac{\Lambda^2 + M_V^2}{M_V^2} \right) \Lambda^2 + \frac{M_V^4}{M^2 - M_V^2} \left[ 2 \left( f_v g V - 2g_v \right) M_A \Lambda^2 \right. \\
\left. - 2 \left( 3 \left( f_v g V - 4g_v \right) M_A \ln \left( \frac{\Lambda^2 + M_A^2}{M_A^2} \right) \right. \right], \tag{B.8}
\]
\[ \tilde{T}^{(V^3B^0A^3, A^2)} \simeq \frac{3\alpha_{em}k^2 f_V^2}{128\pi v^2 M_A^2 \cos^2 \theta_W} \times \left\{ \Lambda^4 + 4 \left(2M_A^2 - M_V^2\right) \Lambda^2 \right. \\
+ \frac{2M_V^4}{(M_A^2 - M_V^2)^2} \left[3M_V^4 + 15M_V^4 \right. \left. - 14M_A^2 M_V^2 \right] \ln \left(\frac{\Lambda^2 + M_V^2}{M_V^2} \right) \\
- \frac{8M_A^8}{(M_A^2 - M_V^2)^2} \ln \left(\frac{\Lambda^2 + M_A^2}{M_A^2} \right) \\
- \frac{2M_A^4 (5M_A^2 - M_V^2)}{(M_A^2 - M_V^2)} \left(\Lambda^2 + M_V^2\right) \right\}, \quad \text{(B.14)} \]

\[ \tilde{T}^{(A^3B^0A^3, V^2)} \simeq \frac{3\alpha_{em}k^2 f_A^2}{128\pi v^2 M_V^2 \cos^2 \theta_W} \times \left\{ \Lambda^4 + 4 \left(2M_V^2 - M_A^2\right) \Lambda^2 \right. \\
+ \frac{2M_A^4}{(M_A^2 - M_V^2)^2} \left[3M_A^4 + 15M_A^4 \right. \left. - 14M_A^2 M_V^2 \right] \ln \left(\frac{\Lambda^2 + M_A^2}{M_A^2} \right) \\
- \frac{8M_A^8}{(M_A^2 - M_V^2)^2} \ln \left(\frac{\Lambda^2 + M_A^2}{M_A^2} \right) \\
- \frac{2M_A^4 (5M_A^2 - M_V^2)}{(M_A^2 - M_V^2)} \left(\Lambda^2 + M_A^2\right) \right\}, \quad \text{(B.15)} \]

\[ \tilde{T}^{(V^3B^0A^3, V^2)} \simeq \frac{3\alpha_{em}k f_V f_A}{64\pi v^2 M_V^2 \cos^2 \theta_W} \times \left\{ \Lambda^4 - 2 \left(M_A^2 - 3M_V^2\right) \Lambda^2 \right. \\
+ \frac{2M_A^4 (M_A^2 - 5M_V^2)}{(M_A^2 - M_V^2)^2} \ln \left(\frac{\Lambda^2 + M_A^2}{M_A^2} \right) \\
+ \frac{2M_V^4}{(M_A^2 - M_V^2)^2} \left[3 \left(M_V^2 - M_A^2\right)^2 \right. \left. - (M_A^2 - 5M_V^2) \left(3M_A^2 - 2M_V^2\right) \right] \ln \left(\frac{\Lambda^2 + M_A^2}{M_A^2} \right) \\
- \frac{8M_A^8 \Lambda^2}{(M_V^2 - M_A^2) \left(\Lambda^2 + M_V^2\right)} \right\}, \quad \text{(B.16)} \]
\( \tilde{T}_{(H^0)} \approx \frac{3 \alpha_{em}}{128 \pi} \left[ \frac{(1 - \kappa)^2 + 2 \kappa^2}{\cos^2 \theta_W} \right] \ln \left( \frac{\Lambda^2}{m_H^2} \right), \quad (B.24) \)

Now, considering the \( S \) parameter, it is defined as \([89, 91–94]\):

\[
S = \frac{4 \sin^2 \theta_W \tilde{S}}{\alpha_{em} (m_Z)} \left( \frac{q^2}{4} \right) \left( \frac{q^2}{4} \right)
\]

where \( \Pi_{30} (q^2) \) is the vacuum polarization amplitude for a loop diagram having \( W^0_3 \) and \( B_\mu \) in the external lines. As before, \( q \) is the external momentum.

Corresponding to the Feynman diagrams shown in Fig. 6, we decompose the \( \tilde{S} \) parameter as

\[
\tilde{S} = \tilde{S}_{(W^3-B^0)} + \tilde{S}_{(\pi^1, \pi^2)} + \tilde{S}_{(\pi^2 V^1)} + \tilde{S}_{(V^1 V^2)} + \tilde{S}_{(V^1 V^2)} + \tilde{S}_{(V^2 V^3)} + \tilde{S}_{(V^3 V^4)}
\]

where the different one-loop contributions are

\[
\tilde{S}_{(W^3-B^0)} = \frac{\pi \alpha_{em} (f^2 - f^2_A - c_{WB})}{\sin^2 \theta_W}, \quad (B.22)
\]

\[
\tilde{S}_{(\pi^1, \pi^2)} \approx \frac{\alpha_{em}}{48 \pi \sin^2 \theta_W} \ln \left( \frac{\Lambda^2}{M^2} \right) + \frac{\alpha_{em} f_Y g_V}{8 \pi \sin^2 \theta_W} \Lambda^2, \quad (B.23)
\]

\[
\tilde{S}_{(V^1 V^2)} = -\frac{\alpha_{em} \Lambda^2}{24 \pi M_Y^2 \sin^2 \theta_W} + \frac{29 \alpha_{em}}{96 \pi \sin^2 \theta_W} \ln \left( \frac{\Lambda^2}{M_Y^2} \right) + \frac{9 \alpha_{em}}{64 \pi \sin^2 \theta_W} - \frac{35 \alpha_{em} \Lambda^2}{96 \pi \left( \Lambda^2 + M_Y^2 \right) \sin^2 \theta_W}
\]

\[
\tilde{S}_{(V^2 V^1)} = \tilde{S}_{(\pi^1 V^2)}, \quad \tilde{S}_{(V^2 A^1)} = \tilde{S}_{(V^1 A^2)}, \quad (B.25)
\]
Fig. 6 One-loop Feynman diagrams contributing to the $S$ parameter

$$S_{(\pi^1V^2)} = -\frac{\alpha_{em}}{256\pi^2 M_V^2 \sin^2 \theta_W} \left[ 6g_V \left(2g_V + \kappa^2 f_V \right) - \frac{16}{3} g_V^2 - 8\kappa^2 f_V g_V \right] \Lambda^4$$

$$+ \frac{\alpha_{em}}{64\pi v^2 \sin^2 \theta_W} \left[ 2 \left(f_V - 2g_V - \kappa^2 f_V \right) \times \left(f_V + 2g_V + \kappa^2 f_V \right) + 14g_V \left(2g_V + \kappa^2 f_V \right) + 16\kappa^2 f_V g_V - \frac{32}{3} g_V^2 \right] \Lambda^2$$

$$- \frac{\alpha_{em}}{64\pi v^2 \sin^2 \theta_W} \int_0^1 dx \left[ 2 \left(f_V - 2g_V - \kappa^2 f_V \right) \times \left(f_V + 2g_V + \kappa^2 f_V \right) + 24g_V \left(2g_V + \kappa^2 f_V \right) x - 12\kappa^2 f_V g_V - 44g_V^2 x^2 \right]$$

$$\times \left[2M_V^2 (1-x) \ln \left(\frac{\Lambda^2 + M_V^2 (1-x)}{M_V^2 (1-x)}\right) - \frac{M_V^2 \Lambda^2 (1-x)}{\Lambda^2 + M_V^2 (1-x)} \right]$$
\[ S_{(V^A)} = \frac{\alpha_{em} \Lambda^2}{24\pi M^2 X^2 \sin^2 \theta_W} + \frac{9 \alpha_{em} \Lambda^2}{96\pi \sin^2 \theta_W} \ln \left( \frac{\Lambda + M^2}{\Lambda X^2} \right) \]

\[ S_{(H^A)} \simeq -\frac{\alpha_{em} \left(1 - \kappa \right)^2}{384\pi \sin^2 \theta_W} \left[ \ln \left( \frac{\Lambda^2}{m^2} \right) - \frac{1}{6} \right], \quad \text{(B.38)} \]

\[ S_{(h^0)} \simeq -\frac{\alpha_{em} \left(1 - \kappa \right)^2 + 2\kappa^2}{384\pi \sin^2 \theta_W} \left[ \ln \left( \frac{\Lambda^2}{m^2} \right) - \frac{1}{6} \right], \quad \text{(B.39)} \]

\[ S_{(A^2)} = \frac{20 \alpha_{em} \kappa^2 (M^2 + M^2_X)}{192\pi M^2 X^2 \sin^2 \theta_W} \Lambda^2 - \frac{9 \alpha_{em} \kappa^2}{64\pi \sin^2 \theta_W} \]

\[ + \frac{5 \alpha_{em} \kappa^2 (M^2 + M^2_X)}{256\pi M^2 X^2 \sin^2 \theta_W} - \frac{\alpha_{em} \kappa^2}{8\pi \sin^2 \theta_W} \int_0^1 dx \left( \chi^2 - x + \frac{5}{2} \right) \]

\[ \times \left[ \ln \left( \frac{\Lambda^2 + M^2}{M^2 - (M^2_X - M^2_X)} x \right) \right] \]

\[ - \frac{\alpha_{em} \kappa^2}{64\pi M^2 X^2 \sin^2 \theta_W} \int_0^1 dx \left[ 10M^2 V \right] \]

\[ + (26x - 3) M^2_A - 13 \left( M^2_A + M^2_X \right) x^2 \]

\[ \times \left[ 2 \left[ \frac{M^2}{M^2 - (M^2_X - M^2_X)} x \right] \right] \]

\[ \times \left[ \ln \left( \frac{\Lambda^2 + \left[ M^2_X - (M^2 - M^2_X) x \right]}{M^2 - (M^2_X - M^2_X) x} \right) \right] \]

\[ - \left[ \frac{M^2}{M^2 - (M^2_X - M^2_X) x} \right] \Lambda^2 \]

\[ + \frac{9 \alpha_{em} \kappa^2}{16\pi \sin^2 \theta_W} \int_0^1 dx \left( 1 - x \right) \]

\[ \times \left[ \ln \left( \frac{\Lambda^2 + \left[ M^2_X - (M^2 - M^2_X) x \right]}{M^2 - (M^2_X - M^2_X) x} \right) \right] \]

\[ - \frac{4 \left[ M^2_X - (M^2_X - M^2_X) x \right] \Lambda^2}{2 (\Lambda^2 + M^2_X - (M^2_X - M^2_X) x)^2} \]

\[ + \frac{3 \left[ M^2_X - (M^2_X - M^2_X) x \right] \Lambda^2}{2 (\Lambda^2 + M^2_X - (M^2_X - M^2_X) x)^2} \]

\[ - \frac{3 \alpha_{em} \kappa^2 (M^2 + M^2_X)}{32\pi M^2 X^2 \sin^2 \theta_W} \int_0^1 dx \left( 1 - x \right) \]

\[ \times \left[ 3 \left[ \frac{M^2}{M^2 - (M^2_X - M^2_X) x} \right] \right] \]

\[ \times \left[ \ln \left( \frac{\Lambda^2 + \left[ M^2_X - (M^2 - M^2_X) x \right]}{M^2 - (M^2_X - M^2_X) x} \right) \right] \]
\[
\hat{S}_{(h^A)} = -\frac{\alpha_{em} \kappa (1 - \kappa) (\sqrt{1 - \kappa} + 2\sqrt{\kappa})^2 M_A^2}{64\pi (M_A^2 - m_h^2)^3 \sin^2 \theta_W} \times \left[ M_A^4 - m_h^4 - 2m_h^2 M_A^2 \ln \left( \frac{M_A^2}{m_h^2} \right) \right], \quad (B.40)
\]
\[
\hat{S}_{(HA)} = -\frac{\alpha_{em} \kappa (1 - \kappa) (\sqrt{1 - \kappa} - 2\sqrt{\kappa})^2 M_A^2}{64\pi (M_A^2 - m_H^2)^3 \sin^2 \theta_W} \times \left[ M_A^4 - m_H^4 - 2m_H^2 M_A^2 \ln \left( \frac{M_A^2}{m_H^2} \right) \right], \quad (B.41)
\]
\[
\hat{S}_{(\eta^3)} = -\frac{\alpha_{em} (1 - \kappa)^2 M_V^2}{32\pi (M_V^2 - m_h^2)^3 \sin^2 \theta_W} \times \left[ M_V^4 - m_h^4 - 2m_h^2 M_V^2 \ln \left( \frac{M_V^2}{m_h^2} \right) \right], \quad (B.42)
\]
\[
\hat{S}_{(\eta^3)} = -\frac{3\alpha_{em} g_C f_v}{64\pi M_V^2 M_A^2 \ln^2 \theta_W} \left[ \Lambda^4 + 2M_V^2 \Lambda^2 - 6M_V^4 \ln \left( \frac{\Lambda^2 + M_V^2}{M_A^2} \right) \right], \quad (B.43)
\]
\[
\hat{S}_{(\eta^3)} = -\frac{3\alpha_{em} g_C f_v}{64\pi M_V^2 M_A^2 \ln^2 \theta_W} \left[ \Lambda^4 + 2M_V^2 \Lambda^2 - 6M_V^4 \ln \left( \frac{\Lambda^2 + M_V^2}{M_A^2} \right) \right], \quad (B.44)
\]
\[
\hat{S}_{(\eta^3)} = -\frac{3\alpha_{em} g_C f_v}{64\pi M_V^2 M_A^2 \ln^2 \theta_W} \left[ \Lambda^4 + 2M_V^2 \Lambda^2 - 6M_V^4 \ln \left( \frac{\Lambda^2 + M_V^2}{M_A^2} \right) \right], \quad (B.45)
\]
\[
\hat{S}_{(\eta^3)} = -\frac{3\alpha_{em} g_C f_v}{64\pi M_V^2 M_A^2 \ln^2 \theta_W} \left[ \Lambda^4 + 2M_V^2 \Lambda^2 - 6M_V^4 \ln \left( \frac{\Lambda^2 + M_V^2}{M_A^2} \right) \right], \quad (B.46)
\]
\[
\hat{S}_{(\eta^3)} = -\frac{3\alpha_{em} g_C f_v}{64\pi M_V^2 M_A^2 \ln^2 \theta_W} \left[ \Lambda^4 + 2M_V^2 \Lambda^2 - 6M_V^4 \ln \left( \frac{\Lambda^2 + M_V^2}{M_A^2} \right) \right], \quad (B.47)
\]
The masses of the scalars $h$ and $H$ and pseudoscalar $\eta$ receive contributions at tree- and at one-loop level corrections. These masses are given by

\begin{align}
    m_h^2 &= (m_h)^2_{\text{tree}} + \Sigma_h, \\
    m_H^2 &= (m_H)^2_{\text{tree}} + \Sigma_H, \\
    m_\eta^2 &= (m_\eta)^2_{\text{tree}} + \Sigma_\eta,
\end{align}

where the tree-level contributions to the parity even and parity odd scalar masses, which are obtained from the scalar potential given in Eq. (A.4) are

\begin{align}
    (m_h^2)^{\text{tree}} &= \frac{v_{\text{LC}}}{4} \left[ (2\kappa_2 + \lambda_3^2) v_{\text{CD}} - 2\sqrt{2} \kappa_3 v_{\text{CD}} \right], \\
    (m_H^2)^{\text{tree}} &= \frac{v_{\text{LC}}}{4} \left[ (2\kappa_2 + \lambda_3^2) v_{\text{CD}} + 2\sqrt{2} \kappa_3 v_{\text{CD}} \right], \\
    (m_\eta^2)^{\text{tree}} &= \frac{v_{\text{LC}}}{4} \left[ (2\kappa_2 + \lambda_3^2) v_{\text{CD}} - 2\sqrt{2} \kappa_3 v_{\text{CD}} \right].
\end{align}

\[\Sigma_h = \Sigma_h^{(\text{spin-0})} + \Sigma_h^{(\text{spin-1/2})} + \Sigma_h^{(\text{spin-1})},\]
\[\Sigma_H = \Sigma_H^{(\text{spin-0})} + \Sigma_H^{(\text{spin-1/2})} + \Sigma_H^{(\text{spin-1})},\]
\[\Sigma_\eta = \Sigma_\eta^{(\text{spin-0})} + \Sigma_\eta^{(\text{spin-1/2})} + \Sigma_\eta^{(\text{spin-1})},\]

These one-loop level contributions come from Feynman diagrams containing spin-0, spin-1/2 and spin-1 particles in the internal lines of the loops. For the contribution from the fermion loops we will only keep the dominant term, which is the one involving the top quark. From the Feynman diagrams shown in Fig. 7, it follows that the spin-0, spin-1/2 and spin-1 particles give the following one-loop level contributions to the masses of the scalars $h$ and $H$ and pseudoscalar $\eta$:

\begin{align}
    \Sigma_h^{(\text{spin-0})} &\simeq 12\lambda_h I_1 (m_h) + 2\lambda_{h^2} H_2 I_1 (m_H) + 2\lambda_{h^2}\eta_2 I_1 (m_\eta), \\
    \Sigma_H^{(\text{spin-0})} &\simeq 12\lambda_H I_1 (m_H) + 2\lambda_{h^2} H_2 I_1 (m_h) + 2\lambda_{h^2}\eta_2 I_1 (m_\eta), \\
    \Sigma_\eta^{(\text{spin-0})} &\simeq 2\lambda_{h^2}\eta_2 I_1 (m_h) + 2\lambda_{h^2}\eta_2 I_1 (m_H). \\
\end{align}

with

\[v_{\text{LC}} = \frac{v}{2\sqrt{1-\kappa}}, \quad v_{\text{CD}} = \frac{v}{2\sqrt{2} \kappa}, \quad \kappa = \frac{M_A^2}{M_A^2},\]

while the one-loop level contributions to the masses of the scalars $h$, $H$ and pseudoscalar $\eta$ can be decomposed as

\[\Sigma_h = \Sigma_h^{(\text{spin-0})} + \Sigma_h^{(\text{spin-1/2})} + \Sigma_h^{(\text{spin-1})},\]
\[\Sigma_H = \Sigma_H^{(\text{spin-0})} + \Sigma_H^{(\text{spin-1/2})} + \Sigma_H^{(\text{spin-1})},\]
\[\Sigma_\eta = \Sigma_\eta^{(\text{spin-0})} + \Sigma_\eta^{(\text{spin-1/2})} + \Sigma_\eta^{(\text{spin-1})},\]

These one-loop level contributions come from Feynman diagrams containing spin-0, spin-1/2 and spin-1 particles in the internal lines of the loops. For the contribution from the fermion loops we will only keep the dominant term, which is the one involving the top quark. From the Feynman diagrams shown in Fig. 7, it follows that the spin-0, spin-1/2 and spin-1 particles give the following one-loop level contributions to the masses of the scalars $h$ and $H$ and pseudoscalar $\eta$:

\begin{align}
    \Sigma_h^{(\text{spin-0})} &\simeq 12\lambda_h I_1 (m_h) + 2\lambda_{h^2} H_2 I_1 (m_H) + 2\lambda_{h^2}\eta_2 I_1 (m_\eta), \\
    \Sigma_H^{(\text{spin-0})} &\simeq 12\lambda_H I_1 (m_H) + 2\lambda_{h^2} H_2 I_1 (m_h) + 2\lambda_{h^2}\eta_2 I_1 (m_\eta), \\
    \Sigma_\eta^{(\text{spin-0})} &\simeq 2\lambda_{h^2}\eta_2 I_1 (m_h) + 2\lambda_{h^2}\eta_2 I_1 (m_H). \\
\end{align}
Fig. 7 One-loop Feynman diagrams in the unitary gauge contributing to the masses of the parity even \( h \) and \( H \) and parity odd \( \eta \) scalars

\[
\Sigma_h^{(\text{spin-1})} \simeq 2a_{WW}^2F_A(M_W) + 2b_{HHWW}F_B(M_W) + 3a_{HA}^2F_A(M_A) + 3b_{HA}F_B(M_A) + J_h(M_W, M_Z, M_A) + \Sigma_{h(RA)}(A) + \Sigma_{h(RZ)}(R) + \Sigma_{h(RV)}(V), \quad (C.17)
\]

\[
\Sigma_\eta^{(\text{spin-1})} \simeq 2b_{\eta WW}F_B(M_W) + b_{\eta WW}F_B(M_Z) + 3a_{\eta VV}F_A(M_V) + 3b_{\eta AA}F_B(M_A) + J_\eta(M_W, M_Z, M_V, M_A) + \Sigma_{\eta(RA)}(A) + \Sigma_{\eta(RZ)}(R) + \Sigma_{\eta(RV)}(V), \quad (C.19)
\]

where the different dimensionless couplings are given by

\[
\lambda_{h^4} = \lambda_{H^4} = \frac{2v_L^2(2k_2 + \lambda_3^2) + v_C^2(2k_2 + 8k_3 + \lambda_3^2)}{1024v_C^2}, \quad (C.20)
\]
\[ \lambda_{h^2H^2} = \frac{6u^2_L c (2\kappa_2 + \lambda_3^2) + v^2_{CD} (6\kappa_2 - 8\kappa_3 + 3\lambda_3^2)}{512v^2_{CD}}, \]  
(C.21)

\[ \lambda_{h^2\eta^2} = \lambda_{H^2\eta^2} = \frac{-2\kappa_2 + 4\kappa_3 + 3\lambda_3^2}{256}, \]  
(C.22)

\[ a_{hWW} = \frac{2\kappa^2 - (1 - \kappa)^2}{2\sqrt{2}}, \quad a_{HWW} = \frac{2\kappa^2 + (1 - \kappa)^2}{2\sqrt{2}}, \]  
(C.23)

\[ a_{hVV} = -\frac{(1 - \kappa)^2}{2\sqrt{2}}, \quad a_{hAA} = \kappa \left( 1 - 2\sqrt{\frac{1 - \kappa}{\kappa}} \right) a_{hVV}, \]  
(C.24)

\[ a_{HVV} = \frac{(1 - \kappa)^2}{2\sqrt{2}}, \quad a_{HAA} = \kappa \left( 1 + 2\sqrt{\frac{1 - \kappa}{\kappa}} \right) a_{HVV}, \]  
(C.25)

\[ b_{hWW} = b_{HHWW} = \frac{(1 - \kappa)^2 + 4\kappa^2}{8}, \quad b_{\eta\eta WW} = \frac{(1 - \kappa)^2}{4}, \]  
(C.26)

\[ b_{hVV} = b_{HHVV} = \frac{1 - \kappa}{8}, \quad b_{hAA} = b_{HAA} = \frac{5\kappa (1 - \kappa)}{4}, \]  
(C.27)

\[ b_{\eta\eta VV} = \frac{1 - \kappa}{4}, \quad b_{\eta\eta AA} = \frac{\kappa (1 - \kappa)}{4}, \]  
(C.28)

and the following loop functions have been introduced:

\[ F_A (M) = \frac{M^4}{v^2} I_A (M), \quad F_B (M) = \frac{M^2}{v^2} I_B (M), \]  
(C.29)

\[ J_h (M_W, M_Z, M_A) = \frac{(1 - \kappa) (\sqrt{1 - \kappa} + 2\sqrt{2} \kappa)^2 M^2_{W \eta \eta}}{2v^2 \cos^2 \theta_W} \times I_{\text{Agen}} (M_Z, M_A) \]  
\[ + \frac{(1 - \kappa) (\sqrt{1 - \kappa} - 2\sqrt{2} \kappa)^2 M^2_{W \eta \eta}}{v^2} \times I_{\text{Agen}} (M_W, M_A), \]  
(C.30)

\[ J_H (M_W, M_Z, M_A) = \frac{(1 - \kappa) (\sqrt{1 - \kappa} + 2\sqrt{2} \kappa)^2 M^2_{W \eta \eta}}{2v^2 \cos^2 \theta_W} \times I_{\text{Agen}} (M_Z, M_A) \]  
\[ + \frac{(1 - \kappa) (\sqrt{1 - \kappa} - 2\sqrt{2} \kappa)^2 M^2_{W \eta \eta}}{v^2} \times I_{\text{Agen}} (M_W, M_A), \]  
(C.31)

\[ J_\eta (M_W, M_Z, M_V, M_A) = \frac{3 (1 - \kappa) M^4_{W \eta}}{v^2} I_{\text{Agen}} (M_V, M_A) \]  
\[ + \frac{(1 - \kappa)^2 M^2_{W \eta} M^2_{V \eta}}{v^2 \cos^2 \theta_W} \times I_{\text{Agen}} (M_Z, M_V) \]  
\[ + \frac{2 (1 - \kappa)^2 M^2_{W \eta} M^2_{V \eta}}{v^2} \times I_{\text{Agen}} (M_W, M_V), \]  
(C.32)

\[ \Sigma_{h(AW)} = \Sigma_{H(AW)} \]  
\[ = \frac{3 (1 - 5\kappa) \sqrt{1 - \kappa} f_A M^2_{W \eta} M^2_{V \eta}}{2v^3} I_{\text{Agen}} (M_W, M_A), \]  
(C.33)

\[ \Sigma_{h(AZ)} = \Sigma_{H(AZ)} \]  
\[ = \frac{3 (1 - 5\kappa) \sqrt{1 - \kappa} f_A M^2_{W \eta} M^2_{V \eta}}{4v^3 \cos \theta_W} I_{\text{Agen}} (M_Z, M_A), \]  
(C.34)

\[ \Sigma_{h(VVV)} = \Sigma_{H(VVV)} \]  
\[ = \frac{6b_{hVV} f^2_{V \eta} M^2_{W \eta} M^2_{V \eta}}{v^4} I_{\text{Agen}} (M_V, M_W), \]  
(C.35)

\[ \Sigma_{h(VZV)} = \Sigma_{H(VZV)} \]  
\[ = \frac{3b_{hVV} f^2_{V \eta} (\cos^2 \theta_W - \sin^2 \theta_W) M^2_{W \eta} M^2_{V \eta}}{v^4 \cos \theta_W} \times I_{\text{Agen}} (M_V, M_Z), \]  
(C.36)

\[ \Sigma_{h(VrV)} = \Sigma_{H(VrV)} \]  
\[ = \frac{6b_{hVV} f^2_{V \eta} \sin \theta_W M^2_{W \eta} M^2_{V \eta}}{v^4} I_4 (M_V), \]  
(C.37)

\[ \Sigma_{h(AWA)} = \Sigma_{H(AWA)} \]  
\[ = \frac{6b_{hAA} f^2_{A \eta} M^2_{W \eta} M^2_{A \eta}}{v^4} I_{\text{Agen}} (M_A, M_W), \]  
(C.38)

\[ \Sigma_{h(AZA)} = \Sigma_{H(AZA)} \]  
\[ = \frac{3b_{hAA} f^2_{A \eta} M^2_{W \eta} M^2_{A \eta}}{v^4 \cos \theta_W} I_{\text{Agen}} (M_A, M_Z), \]  
(C.39)

\[ \Sigma_{\eta(AW)} = \frac{3 (1 - \kappa) \sqrt{1 - \kappa} f_A M^2_{W \eta} M^2_{V \eta}}{v^3} I_{\text{Agen}} (M_W, M_A), \]  
(C.40)

\[ \Sigma_{\eta(AZ)} = \frac{3 (1 - \kappa) \sqrt{1 - \kappa} f_A M^2_{W \eta} M^2_{V \eta}}{2v^3 \cos \theta_W} I_{\text{Agen}} (M_W, M_A). \]  
(C.41)
\[ \Sigma_{\eta(VWV)} = \frac{6b_{\eta V V} f_{V}^{2} M_{W}^{2} M_{V}^{2}}{v^{4}} \ln \left( \frac{M_{W}^{2}}{M^{2}} \right), \quad \text{(C.42)} \]

\[ \Sigma_{\eta(VZV)} = \frac{3b_{\eta V V} f_{V}^{2} (\cos^{2} \theta_{W} - \sin^{2} \theta_{W}) M_{W}^{2} M_{V}^{2}}{v^{4} \cos \theta_{W}} \times I_{6\text{gen}}(M_{V}, M_{Z}), \quad \text{(C.43)} \]

\[ \Sigma_{\eta(VVV)} = \frac{6b_{\eta V V} f_{V}^{2} \sin \theta_{W} M_{W}^{2} M_{V}^{2}}{v^{4}} I_{4}(M_{V}), \quad \text{(C.44)} \]

\[ \Sigma_{\eta(AWA)} = \frac{6b_{\eta A A} f_{A}^{2} M_{W}^{2} M_{A}^{2}}{v^{4}} I_{6\text{gen}}(M_{A}, M_{W}), \quad \text{(C.45)} \]

\[ \Sigma_{\eta(AZA)} = \frac{3b_{\eta A A} f_{A}^{2} M_{W}^{2} M_{A}^{2}}{v^{4} \cos \theta_{W}} I_{6\text{gen}}(M_{A}, M_{Z}), \quad \text{(C.46)} \]

\[ I_{B}(M) = 4I_{1}(M) - \frac{1}{M^{2}} I_{2}(M), \quad \text{(C.47)} \]

\[ I_{1}(M) = - \frac{1}{16\pi^{2}} \left[ \Lambda^{2} - M^{2} \ln \left( \frac{\Lambda^{2} + M^{2}}{M^{2}} \right) \right], \quad \text{(C.48)} \]

\[ I_{2}(M) = \frac{1}{32\pi^{2}} \Lambda^{4} - \frac{M^{2}}{16\pi^{2}} \left[ \Lambda^{2} - M^{2} \ln \left( \frac{\Lambda^{2} + M^{2}}{M^{2}} \right) \right], \quad \text{(C.49)} \]

\[ I_{A}(M) = 4I_{3}(M) - \frac{2}{M^{2}} I_{4}(M) + \frac{1}{M^{4}} I_{5}(M), \quad \text{(C.50)} \]

\[ I_{3}(M) = \frac{1}{16\pi^{2}} \left[ \ln \left( \frac{\Lambda^{2} + M^{2}}{M^{2}} \right) - \frac{\Lambda^{2}}{\Lambda^{2} + M^{2}} \right], \quad \text{(C.51)} \]

\[ I_{4}(M) = - \frac{1}{16\pi^{2}} \left[ \Lambda^{2} - 2M^{2} \ln \left( \frac{\Lambda^{2} + M^{2}}{M^{2}} \right) + \frac{M^{2} \Lambda^{2}}{\Lambda^{2} + M^{2}} \right], \quad \text{(C.52)} \]

\[ I_{5}(M) = \frac{1}{32\pi^{2}} \left[ \Lambda^{4} - 4M^{2} \Lambda^{2} + 6M^{4} \ln \left( \frac{\Lambda^{2} + M^{2}}{M^{2}} \right) - \frac{2M^{4} \Lambda^{2}}{\Lambda^{2} + M^{2}} \right], \quad \text{(C.53)} \]

\[ I_{6\text{gen}}(M_{1}, M_{2}) = 4I_{3\text{gen}}(M_{1}, M_{2}) - \left( \frac{1}{M_{1}^{2}} + \frac{1}{M_{2}^{2}} \right) I_{4\text{gen}}(M_{1}, M_{2}) + \frac{1}{M_{1}^{2} M_{2}^{2}} I_{5\text{gen}}(M_{1}, M_{2}), \quad \text{(C.54)} \]

\[ I_{3\text{gen}}(M_{1}, M_{2}) = \frac{1}{16\pi^{2}} \left[ \frac{M_{1}^{2}}{M_{1}^{2} - M_{2}^{2}} \ln \left( \frac{\Lambda^{2} + M_{1}^{2}}{M_{1}^{2}} \right) + \frac{M_{2}^{2}}{M_{2}^{2} - M_{1}^{2}} \ln \left( \frac{\Lambda^{2} + M_{2}^{2}}{M_{2}^{2}} \right) \right], \quad \text{(C.55)} \]

\[ I_{4\text{gen}}(M_{1}, M_{2}) = - \frac{1}{16\pi^{2}} \left[ \frac{\Lambda^{2}}{M_{1}^{2} - M_{2}^{2}} \ln \left( \frac{\Lambda^{2} + M_{1}^{2}}{M_{1}^{2}} \right) - \frac{M_{2}^{2}}{M_{2}^{2} - M_{1}^{2}} \ln \left( \frac{\Lambda^{2} + M_{2}^{2}}{M_{2}^{2}} \right) \right], \quad \text{(C.56)} \]

\[ I_{5\text{gen}}(M_{1}, M_{2}) = \frac{1}{32\pi^{2}} \left[ \frac{M_{1}^{2}}{M_{1}^{2} - M_{2}^{2}} \ln \left( \frac{\Lambda^{2} + M_{1}^{2}}{M_{1}^{2}} \right) + \frac{M_{2}^{6}}{M_{2}^{2} - M_{1}^{2}} \ln \left( \frac{\Lambda^{2} + M_{2}^{2}}{M_{2}^{2}} \right) \right], \quad \text{(C.57)} \]

\[ I_{6\text{gen}}(M_{1}, M_{2}) = - \frac{1}{16\pi^{2}} \left[ \frac{\Lambda^{2}}{M_{1}^{2} - M_{2}^{2}} \ln \left( \frac{\Lambda^{2} + M_{1}^{2}}{M_{1}^{2}} \right) + \frac{M_{2}^{6}}{M_{2}^{2} - M_{2}^{2}} \ln \left( \frac{\Lambda^{2} + M_{2}^{2}}{M_{2}^{2}} \right) \right], \quad \text{(C.58)} \]

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